A UNIVERSAL, TURBULENCE-REGULATED STAR FORMATION LAW: FROM MILKY WAY CLOUDS TO HIGH-REDSHIFT DISK AND STARBURST GALAXIES

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Received 2015 March 16; accepted 2015 May 9; published 2015 June 22

ABSTRACT

While the star formation rate (SFR) of molecular clouds and galaxies is key in understanding galaxy evolution, the physical processes that determine the SFR remain unclear. This uncertainty about the underlying physics has resulted in various different star formation (SF) laws, all having substantial intrinsic scatter. Extending upon previous works that define the column density of star formation ($\Sigma_{\text{SFR}}$) by the gas column density ($\Sigma_{\text{gas}}$), we develop a new universal SF law based on the multi-freefall prescription of gas. This new SF law relies primarily on the probability density function and on the sonic Mach number of the turbulence in the star-forming clouds. By doing so we derive a relation where the SFR correlates with the molecular gas mass per multi-freefall time, whereas previous models had used the average, single-freefall time. We define a new quantity called maximum (multi-freefall) gas consumption rate (MGCR) and show that the actual SFR is only about 0.4% of this maximum possible SFR, confirming the observed low efficiency of SF. We show that placing observations in this new framework ($\Sigma_{\text{SFR}}$ versus MGCR) yields a significantly improved correlation with 3–4 times reduced scatter compared to previous SF laws and a goodness-of-fit parameter $R^2 = 0.97$. By inverting our new relationship, we provide sonic Mach number predictions for kiloparsec-scale observations of Local Group galaxies as well as unresolved observations of local and high-redshift disk and starburst galaxies that do not have independent, reliable estimates for the turbulent cloud Mach number.

Key words: galaxies: high-redshift – galaxies: ISM – galaxies: starburst – ISM: clouds – stars: formation – turbulence

1. INTRODUCTION

The evolution of galaxies is driven by the intricate power play between interstellar turbulence and gravity controlling the formation of stars in giant molecular clouds (Ferrière 2001; Elmegreen & Scalo 2004; Mac Low & Klessen 2004; McKee & Ostriker 2007; Padoan et al. 2014, p. 77). The rate at which stars form is hence a pivotal quantity in tracing a galaxy’s fundamental properties and distribution of matter and activity. Nonetheless, the functional dependence of the column density of SF ($\Sigma_{\text{SFR}}$) has been a highly debated topic for more than two decades, with historical parameterizations including the mean column density of available gas ($\Sigma_{\text{gas}}$; Schmidt 1959; Kennicutt 1998; Bigiel et al. 2008; Leroy et al. 2008; Daddi et al. 2010; Schruba et al. 2011; Kennicutt & Evans 2012; Renaud et al. 2012), as well as the ratio between $\Sigma_{\text{gas}}$ and the mean freefall time $t_{\text{ff}}$ (Krumholz et al. 2012; Federrath 2013; Krumholz 2014). However, significant scatter remains in both these approaches, such that $\Sigma_{\text{SFR}}$ can vary by more than an order of magnitude for any given input $\Sigma_{\text{gas}}$ or $\Sigma_{\text{gas}}/t_{\text{ff}}$. Follow-up analyses of these theoretical models via computer simulations have determined that the observed scatter may be primarily attributed to the physical variations in the sonic Mach number ($M$) of the turbulence in the star-forming clouds (Federrath 2013). This results in separate $M$-dependent relations for the SFR, which cover the observed range of $\Sigma_{\text{SFR}}$. The aim of this work is hence to unify these separate laws and develop a unique, universal relation.

In Section 2 we introduce and derive our new SF law based on the probability density function (PDF) and Mach number of interstellar turbulence. Section 3 describes the observational sample utilized to assess our new SF law. In Section 4 we present our findings and compare our new model to previous parameterizations. In Section 5 we invert our new SF law to make sonic Mach number predictions for extragalactic sources. Finally, Section 6 summarizes our conclusions.

2. A NEW SFR DESCRIPTOR

Here we derive an improved SF law, which takes into account the distribution of gas densities (PDF) present in galactic clouds and the interstellar medium (ISM). This follows from the finding that the observed scatter in the SF law can be principally attributed to the variation in the sonic Mach number of the clouds and galaxies observed (Federrath 2013).

2.1. The PDF of Interstellar Gas

In 2012 Krumholz, Dekel, and McKee initiated the refinement of the traditional Kennicutt–Schmidt law by dividing the gas surface density by the freefall time of the gas ($\Sigma_{\text{gas}}/t_{\text{ff}}$), indeed achieving a stark improvement in star formation rate correlation (Krumholz et al. 2012; Federrath 2013; Krumholz 2014). However, because this model implements only the division between the average surface density and the average freefall time of the gas, important information regarding the wide distribution of densities within the ISM and molecular clouds (Kainulainen et al. 2009, 2013, 2014; Schneider et al. 2012, 2013) is not taken into account. We hence extend upon the important previous work by Krumholz et al. (2012) to incorporate the density PDF, with the ultimate goal of eliminating the remaining scatter in the previous relation.

In our new SF law, we must consider the fact that denser gas forms stars at a higher rate (Silk 1997; Krumholz & McKee 2005; Padoan & Nordlund 2011; Hopkins 2013) because gas with higher density $\rho$ has a shorter freefall time.
than more diffuse gas,
\[
t_f(\rho) = \sqrt{\frac{3\pi}{32G\rho}},
\]
where \( G \) is the gravitational constant. Note that the concept of a multi-freefall time was pioneered by Hennebelle & Chabrier (2011, 2013) and Chabrier et al. (2014). It suggests that due to the clumpy nature of molecular clouds, the typical timescale for SF is not the average timescale of the clouds, but the density-dependent timescale of each collapsing substructure within the clouds. This multi-freefall concept has recently received support from numerical simulations in Federrath & Klessen (2012) and from observations in Evans et al. (2014).

In contrast, Krumholz et al. (2012) and Federrath (2013) had only correlated \( \Sigma_{\text{SFR}} \) with \( \Sigma_{\text{gas}}(\rho_0)/t_f(\rho_0) \) (hence denoted as \( \Sigma_{\text{gas}/f}, \) i.e., only at a single freefall time evaluated at the mean density \( \rho_0 \). It is conceivable, however, that the true correlation must be in the form of an integral over the whole density PDF, \( \int \Sigma_{\text{gas}}(\rho)/t_f(\rho_1)(\rho) d\rho \). In the following, we compute this integral by making the standard assumption that the PDF follows a log-normal distribution as the initial condition for SF:

\[
p(s)ds = \frac{1}{\sqrt{2\pi}\sigma_s^2} \exp\left(-\frac{(s-s_0)^2}{2\sigma_s^2}\right) ds,
\]
where the density is written in logarithmic form, normalized to the mean density
\[
s = \ln(\rho/\rho_0).
\]
This transformation of variables from \( \rho \) to \( s \) has advantages during the integration step below and allows us to write the PDF, Equation (2), in its standard log-normal form. The mean logarithmic density \( s_0 \) is related to the variance \( \sigma_s^2 \) by
\[
s_0 = -\sigma_s^2/2 \quad (\text{Vázquez-Semadeni 1994}).
\] As derived by Padoan & Nordlund (2011) and Molina et al. (2012), the logarithmic density variance is given by
\[
\sigma_s^2 = \ln \left( 1 + b^2 \mathcal{M}^3 \frac{\beta}{\beta + 1} \right),
\]
parameterized by the sonic Mach number \( \mathcal{M} \), the turbulent driving parameter \( b \) (Federrath et al. 2008, 2010), and the ratio of thermal to magnetic pressure, plasma \( \beta \).

The log-normal PDF, Equation (2), and the associated density variance—Mach number relation, Equation (4), are observed to provide a good approximation to the real PDF in molecular clouds (Kainulainen et al. 2009, 2014; Brunt 2010; Schneider et al. 2012, 2013), in the Galactic center (Rathborne et al. 2014), on large Galactic scales (Berkhuijsen & Fletcher 2008), and even in extra-galactic systems (Hughes et al. 2013; Berkhuijsen & Fletcher 2015).

\[2.2. \text{Derivation of the Maximum (Multi-freefall) Gas Consumption Rate}\]

For a rigorous derivation, we start by defining a cartesian coordinate system in which the line of sight toward the cloud or galaxy is in the \( z \)-direction and maps of column density and SFR surface density are in the \( xy \)-plane. First, the gas column density is defined as \( \Sigma_{\text{gas}}(\rho) = \int_{\rho} H_z^2 \rho dz \), where \( H_z \) is the scale height of the cloud or galaxy; for which \( \Sigma_{\text{gas}} \) is to be determined. From observations and simulations discussed in the previous section, we know that \( \Sigma_{\text{gas}} \) and \( \rho \) follow closely a log-normal distribution, Equation (2). Thus, in order to compute an average of a density-dependent variable, we simply have to integrate that variable over the entire PDF. For the average gas column density, for example, we would evaluate
\[
\Sigma_{\text{gas}}/\Sigma_{\text{gas}} = \int \rho \rho_0 d\rho ds = \int \rho \exp(s) \rho_0 ds dz = \rho_0 \int dz = \rho_0 H_z,
\]
which is indeed the average column density \( \Sigma_{\text{gas}}(\rho_0) \). Now we follow exactly the same mathematical procedure, but for the combined density-dependent variable \( \Sigma_{\text{gas}}/t_f = \Sigma_{\text{gas}}(\rho_0)/t_f(\rho_0) \exp(s/2) \), i.e.,

\[
\Sigma_{\text{gas}}/t_f = \Sigma_{\text{gas}}(\rho_0)/t_f(\rho_0) \exp(s/2) = \int \rho \rho_0 \exp(s) \rho_0 d\rho ds dz = \rho_0 \int dz = \rho_0 H_z,
\]
the third step transforms variables from \( \rho \) to \( s \) via Equation (3) and via the identity \( \rho \rho_0 = s \rho_0 ds \). The last step, Equation (8), is the analytic solution of the integral over all densities.

We call this new quantity derived above, the maximum gas consumption rate or multi-freefall gas consumption rate (MGCR), denoted \( \Sigma_{\text{gas/ft}} \).
single-freefall average $\Sigma_{\text{gas}}(\rho_0)/t_{\text{ff}}(\rho_0) \equiv (\Sigma_{\text{gas}}/t)_{\text{single-ff}}$ used in Krumholz et al. (2012) and Federrath (2013) for the underlying PDF of densities.

We can now insert the density variance from Equation (4) into Equation (8) and obtain the multi-freefall correction factor,

$$C_{\text{multi-ff}} \equiv \left( \frac{\Sigma_{\text{gas}}/t}{\Sigma_{\text{gas}}/t}_{\text{single-ff}} \right)_{\text{multi-ff}} = \left( 1 + b^2 M^2 \frac{\beta}{\beta + 1} \right)^{3/8}. \tag{9}$$

Figure 1 shows the $(\Sigma_{\text{gas}}/t)_{\text{multi-ff}}/(\Sigma_{\text{gas}}/t)_{\text{single-ff}}$ correction factor, Equation (9), as a function of the Mach number $M$ for three values of the turbulent driving parameter $b$ and—for simplicity—neglecting magnetic fields, i.e., $\beta \rightarrow \infty$. We see that the multi-freefall correction is always positive and increases with increasing Mach number. The correction factor is about an order of magnitude for typical cloud Mach numbers, $M \sim 5–50$, which means that our correction to the previous SF laws will be significant. In the following, we will assume a fixed turbulent driving parameter, $b = 0.4$, representing a natural mixture. However, we emphasize that $b$ is not likely fixed across all molecular clouds (Brunt 2010; Price et al. 2011; Ginsburg et al. 2013; Kainulainen et al. 2014), but in the absence of a direct measurement of $b$, we presume a standard value for all clouds.

3. OBSERVATIONAL SAMPLE SELECTION

We selected our sample of 11 galactic objects and 1 extragalactic object based on the availability of gas or dust column density ($\Sigma_{\text{gas}}$) and SFR column density ($\Sigma_{\text{SFR}}$). Submillimeter observations are the primary source for the study of molecular gas clouds in galaxies. In combination with young stellar object (YSO) counts, infrared and ultraviolet luminosities, $\Sigma_{\text{SFR}}$ measurements may be obtained. As our new SFR descriptor is primarily dependent on the sonic Mach number of the gas in each observed source, availability of such estimates were vital in selecting relevant data. Mach number estimates for Milky Way clouds (Heiderman et al. 2010; Lada et al. 2010; Gutermuth et al. 2011), molecular clumps (Wu et al. 2010), YSO (Heiderman et al. 2010) and the Central Molecular Zone (CMZ; Yusef-Zadeh et al. 2009) as well as the SMC (Bolatto et al. 2011) were taken from and are summarized in Federrath (2013). A summary of the data and sonic Mach number estimates utilized are listed in Table 1. Derivation of $(\Sigma_{\text{gas}}/t)_{\text{multi-ff}}$ was calculated via Equation (9) using $b = 0.4$ and $\beta \rightarrow \infty$ for all cases except the Taurus molecular cloud. Taurus is known to exhibit high levels of magnetic activity (Heyer & Brunt 2012), so an estimate of $\beta = 2M_A^2/M^2 \sim 0.02$ (with the sonic and Alfvén Mach number, $M = 10$ and $M_A = 1$, respectively; see Heyer & Brunt 2012) was applied to obtain Taurus’s multi-freefall correction factor.

Previous SF laws have reported data points attained from individual clouds and assigned a linear correlation between $\Sigma_{\text{SFR}}$ and $\Sigma_{\text{gas}}$ or $(\Sigma_{\text{gas}}/t)_{\text{single-ff}}$ (Kennicutt & Evans 2012; Krumholz et al. 2012). However, because we do not have sonic Mach number measurements for individual clouds, utilizing the data points from each cloud to derive a law from our new descriptor would not be an accurate method of derivation. We can only obtain approximate values of sonic Mach number for populations of clouds, so in order to arrive at a fair comparison for each relation we report the geometric mean values of $\Sigma_{\text{SFR}}$, $\Sigma_{\text{gas}}$, $(\Sigma_{\text{gas}}/t)_{\text{single-ff}}$, and $M$ for each group of clouds and apply robust line fits to these data points. The error bars associated with each point were derived from calculating the standard deviation of the mean. Since the previous SFR descriptors $\Sigma_{\text{gas}}$ and $(\Sigma_{\text{gas}}/t)_{\text{single-ff}}$ do not depend on the sonic Mach number of...
the clouds, uncertainty in the values of $M$ was not propagated when deriving values of $(\Sigma_{\text{gas}}/\dot{t})_{\text{multi-ff}}$ in order to objectively evaluate differences between our new SFR descriptor and previous works.

4. RESULTS: AN IMPROVED SF LAW

Figure 2 shows a direct comparison of previous SF laws, $\Sigma_{\text{SFR}}$ versus $\Sigma_{\text{gas}}$ (left panel) and $\Sigma_{\text{SFR}}$ versus $(\Sigma_{\text{gas}}/\dot{t})_{\text{single-ff}}$ (middle panel), together with our new MGCR correlator, $\Sigma_{\text{SFR}}$ versus $(\Sigma_{\text{gas}}/\dot{t})_{\text{multi-ff}}$ (right panel), including all the data listed in Table 1. For the classical Kennicutt–Schmidt relation (left-hand panel), we apply a two-parameter robust power-law fit, with the offset and the slope of the power law as free parameters. For the Krumholz et al. (2012) relation (middle panel) and for our new multi-freefall relation (right-hand panel), we respectively apply a one-parameter robust fit with the offset as the only free parameter (the slope is fixed to unity). Thus, both the Krumholz et al. (2012) single-freefall SF law and our new multi-freefall SF law predict a direct linear relationship between the actual SFR and the maximum possible single-freefall or maximum possible multi-freefall gas consumption rate, respectively. We also apply the two-parameter robust fit to both these relations in order to gauge how much they deviate from the assumed unity slope.

In order to quantitatively evaluate the relative goodness of fit for each relation, we have applied two statistical tests to the data generated by each parameterization and their corresponding lines of best fits, summarized in Table 2. The first value, which we define as the relative scatter in each relation, is the unweighted $\chi^2$ value normalized with respect to our new SFR descriptor, $(\Sigma_{\text{gas}}/\dot{t})_{\text{multi-ff}}$. Scatter values greater than unity hence indicate a greater degree of scatter than that present in our new relation. The second test applied attains a value for the goodness-of-fit, $R^2$. The $R^2$ value is the coefficient of determination and has a range of 0–1. An $R^2 = 1$ indicates a model that perfectly fits the data.

Both the statistical tests we have applied show a significantly tighter correlation between $\Sigma_{\text{SFR}}$ and $(\Sigma_{\text{gas}}/\dot{t})_{\text{multi-ff}}$ than with either $(\Sigma_{\text{gas}}/\dot{t})_{\text{single-ff}}$ or $\Sigma_{\text{gas}}$, as summarized in Table 2. For the $(\Sigma_{\text{gas}}/\dot{t})_{\text{single-ff}}$ and $(\Sigma_{\text{gas}}/\dot{t})_{\text{multi-ff}}$ parameterizations, this conclusion is further emphasized by the behavior of their residuals and gradients of their two parameter least-squares fits. The two-
Table 2

Summary of the Results of the Statistical Tests Applied to the Data and the Fits Generated to Model Their Relationship

| log_{10} Σ_{SFR} Correlator | Offset | Slope | Scatter | R² |
|-----------------------------|--------|-------|---------|----|
| Two-parameter fits          |        |       |         |    |
| log_{10} Σ_{gas}            | −3.70  | 1.70 ± 0.21 | 3.83 | 0.864 |
| log_{10} (Σ_{gas}/t)_{singe-ff} | −1.61 | 0.78 ± 0.05 | 1.07 | 0.962 |
| log_{10} (Σ_{gas}/t)_{multi-ff} | −2.37 | 1.01 ± 0.06 | 0.99 | 0.965 |
| One-parameter fits          |        |       |         |    |
| log_{10} (Σ_{gas}/t)_{singe-ff} | −1.99 | 1 (fixed) | 3.34 | 0.881 |
| log_{10} (Σ_{gas}/t)_{multi-ff} | −2.34 | 1 (fixed) | 1.00 | 0.965 |

Notes. Column 1: SFR descriptor in log space. Column 2: offset of the relation’s robust line fit in log space. Column 3: slope of the relation’s robust line fit in log space. Column 4: relative scatter of the data. Column 5: goodness-of-fit, R² value (R² = 1 would indicate a perfect fit).

5. APPLICATION OF THE NEW MODEL: MACH NUMBER PREDICTIONS FOR EXTRAGALACTIC SOURCES

The Krumholz et al. (2012) SF law had utilized extragalactic data of disk and starburst galaxies (Kennicutt 1998; Bouché et al. 2007; Daddi et al. 2010; Genzel et al. 2010; Tacconi et al. 2010) in addition to Milky Way observations. However, it is difficult to accurately gauge the values of $M_*$ for extragalactic sources as we are not able to well resolve individual molecular clouds, especially at high redshifts. $M_*$ estimates require measurements of the sound speed and turbulent velocity dispersion of a cloud, which in turn requires high-resolution molecular line data and a temperature measurement. Such data are hard to obtain for molecular clouds in external galaxies, as a complete census of the star-forming molecular cloud population in a given galaxy is needed at sufficiently high resolution to capture the cloud-scale Mach number. There are only very few studies of nearby galaxies (such as M51) that start to resolve molecular clouds in external galaxies (Hughes et al. 2013), but even those do not necessarily yield a complete census of clouds and it is not clear that all cloud properties are converged at the telescope resolutions available to date.

We were hence unable to include extragalactic sources that lack $M_*$ estimates in the deduction of our new SF law. They were similarly omitted in our analysis of previous laws in order to arrive at a fair comparison between the different parameterizations of $Σ_{SFR}$ in Figure 2 and Table 2. Instead, we invert our new model, Equation (10), in order to compute $M_*$ estimates for these extragalactic sources; predictions to be tested by future observations of resolved CO maps in extragalactic sources. Our $M_*$ predictions are summarized in Table 3. Since the presence of vigorous SF in starburst galaxies would result in more violent turbulence of gas compared to disk galaxies, it is expected that the starburst galaxies have greater $M_*$ than their disk galaxy counterparts of the same redshift range, which is indeed the systematic trend we find in Table 3. This trend is consistent with the analyses and conclusions presented in Chabrier et al. (2014).

Table 3

Mach Number Predictions for Extragalactic Systems Obtained by Inverting Our Improved SF Law, Equation (10)

| Data Source | Redshift | Galaxy Type | $M_*$ Estimate |
|-------------|----------|-------------|----------------|
| Kennicutt (1998) | ~0        | Disk        | 4.0$_{-1.7}^{+2.0}$  |
| Daddi et al. (2010) | 1–3     | Disk        | 16$_{-11}^{+24}$  |
| Tacconi et al. (2010) | 1–3   | Disk        | 18$_{-10}^{+27}$  |
| Genzel et al. (2010) | 1–3    | Starburst   | 5.7$_{-4.0}^{+1.4}$  |
| Bouché et al. (2007) | 1–3   | Starburst   | 71$_{-30}^{+10}$  |

Notes. Column 1: reference. Column 2: redshift range. Column 3: galaxy type. Column 4: geometric mean $M_*$ prediction from inverting the improved SF law, Equation (10), as well as the upper and lower limits of this $M_*$ estimate.

6. CONCLUSIONS

We derived a new SF law given by Equation (10), which is based primarily on the sonic Mach number of turbulence, as a
result of the density PDF of molecular, star-forming gas clouds. We find that the SFR is equal to ~0.4% of the MGCR, which we derived in Section 2. We compared our new model to previous parameterizations of the SFR and determined quantitatively that our new SF law provides a tight linear relation between $SFR$ and MGCR, with a factor of 3–4 less scatter compared to any previous SF law. By inverting Equation (10), we predict the Mach numbers ($\mathcal{M}$) of the star-forming molecular clouds in extragalactic sources. Our predictions are summarized in Table 3, which anticipate testing via future submillimeter observations.

We thank Christopher McKee and the anonymous referee for useful comments, which improved this work. C.F. acknowledges funding provided by the Australian Research Council’s (ARC) Discovery Projects (grants DP130102078 and DP150104329). L.J.K. gratefully acknowledges the support of an ARC Future Fellowship and ARC Discovery Project DP130103925.

REFERENCES

Berkhuijsen, E. M., & Fletcher, A. 2008, MNRAS, 390, L19  
Berkhuijsen, E. M., & Fletcher, A. 2015, MNRAS, 448, 2469  
Bigiel, F., Leroy, A., Walter, F., et al. 2008, AJ, 136, 2846  
Bolatto, A. D., Leroy, A. K., Jameson, K., et al. 2011, ApJ, 741, 12  
Bouché, N., Cresci, G., Davies, R., et al. 2007, ApJ, 671, 303  
Brunt, C. M. 2010, A&A, 513, A67  
Chabrier, G., Hennebelle, P., & Charlot, S. 2014, ApJ, 796, 75  
Daddi, E., Elbaz, D., Walter, F., et al. 2010, ApJL, 714, L118  
Elmegreen, B. G., & Scalo, J. 2004, ARA&A, 42, 211  
Evans, N. J., II, Heiderman, A., & Vutisalchavakul, N. 2014, ApJ, 782, 114  
Federrath, C. 2013, MNRAS, 436, 3167  
Federrath, C., & Klessen, R. S. 2012, ApJ, 761, 156  
Federrath, C., Klessen, R. S., & Schmidt, W. 2008, ApJL, 688, L79  
Federrath, C., Roman-Duval, J., Klessen, R. S., Schmidt, W., & Mac Low, M. 2010, A&A, 512, A81  
Ferrière, K. M. 2001, RvMP, 73, 1031  
Genzel, R., Tacconi, L. J., Gracia-Carpio, J., et al. 2010, MNRAS, 407, 2091  
Ginsburg, A., Federrath, C., & Darling, J. 2013, ApJ, 779, 50  
Getternuth, R. A., Pipper, J. L., Megeath, S. T., et al. 2011, ApJ, 739, 84  
Heiderman, A., Evans, N. J., II, Allen, L. E., Huard, T., & Heyer, M. 2010, ApJ, 723, 1019  
Hennebelle, P., & Chabrier, G. 2011, ApJL, 743, L29  
Hennebelle, P., & Chabrier, G. 2013, ApJ, 770, 150  
Heyer, M. H., & Brunt, C. M. 2012, MNRAS, 420, 1562  
Hopkins, P. F. 2013, MNRAS, 430, 1653  
Hugues, A., Meidt, S. E., Schinnerer, E., et al. 2013, ApJ, 779, 44  
Kainulainen, J., Beuther, H., Henning, T., & Plume, R. 2009, A&A, 508, L35  
Kainulainen, J., Federrath, C., & Henning, T. 2013, A&A, 553, L8  
Kainulainen, J., Federrath, C., & Henning, T. 2014, Sci, 344, 183  
Kennicutt, R. C., Jr. 1998, ApJ, 498, 541  
Kennicutt, R. C., & Evans, N. J. 2012, ARA&A, 50, 531  
Krumholz, M. R. 2014, PhR, 539, 49  
Krumholz, M. R., Dekel, A., & McKee, C. F. 2012, ApJ, 745, 69  
Krumholz, M. R., & McKee, C. F. 2005, ApJ, 630, 250  
Lada, C. J., Lombardi, M., & Alves, J. F. 2010, ApJ, 724, 687  
Leroy, A. K., Walter, F., Brinks, E., et al. 2008, AJ, 136, 2782  
Mac Low, M.-M., & Klessen, R. S. 2004, RvMP, 76, 125  
McKee, C. F., & Ostriker, E. C. 2007, A&A, 45, 565  
Molina, F. Z., Glover, S. C. O., Federrath, C., & Klessen, R. S. 2012, MNRAS, 423, 2680  
Padoan, P., Federrath, C., Chabrier, G., et al. 2014, in Protostars and Planets VI, ed. H. Beuther et al. (Tucson, AZ: Univ. Arizona Press), 77  
Padoan, P., & Nordlund, Å. 2011, ApJ, 730, 40  
Price, D. J., Federrath, C., & Brunt, C. M. 2011, ApJL, 727, L21  
Rathborne, J. M., Longmore, S. N., Jackson, J. M., et al. 2014, ApJL, 795, L25  
Renaud, F., Kraljic, K., & Bournaud, F. 2012, ApJL, 760, L16  
Schmidt, M. 1959, ApJ, 129, 243  
Schneider, N., André, P., Könyves, V., et al. 2013, ApJ, 766, L17  
Schneider, N., Csengeri, T., Hennemann, M., et al. 2012, A&A, 540, L11  
Schruba, A., Leroy, A. K., Walter, F., et al. 2011, AJ, 142, 27  
Silk, J. 1997, ApJ, 481, 703  
Tacconi, L. J., Genzel, R., Neri, R., et al. 2010, Natur, 463, 781  
Vázquez-Semadeni, E. 1994, ApJ, 432, 681  
Wu, J., Evans, N. J., II, Shirley, Y. L., & Knez, C. 2010, ApJS, 188, 313  
Yusef-Zadeh, F., Hewitt, J. W., Arendt, R. G., et al. 2009, ApJ, 702, 178