The Higgs boson is the only Standard Model (SM) particle that remains elusive. The next runs at the Fermilab Tevatron have the potential for discovering the Higgs boson for a mass range beyond the current LEP limit. Remarkable efforts have been devoted to designing the best search strategy for a SM-like Higgs boson, with a large branching into $b$-jets or $W$-bosons. However, a Higgs boson, $h^0$, with SM-like couplings to the gauge bosons and fermions, could nevertheless have decay modes dramatically different from the SM ones. The reason is that the SM is likely to be a part of a more comprehensive theory which may include an extended Higgs sector. It is then possible for the Higgs boson to decay into pairs of other neutral scalars, whenever they are lighter than half the $h^0$ mass, $M_h$.

An example of such an extended Higgs sector is given by the Minimal Composite Higgs Model (MCHM), which is based on the top-quark condensation seesaw mechanism. At low energy, the MCHM includes two composite Higgs doublets and two gauge-singlet scalars, with the $h^0$ and a CP-odd scalar, $A^0$, being the lightest scalar mass eigenstates. Another interesting example is the Next-to-Minimal Supersymmetric Standard Model (NMSSM), where the presence of two Higgs doublets and a gauge singlet allows a region of parameter space in which $M_h$ is larger than twice the mass $M_A$ of the lightest CP-odd scalar, $A^0$. Both in the MCHM and NMSSM it is natural to have a light $A^0$ because its mass is controlled by the explicit breaking of a spontaneously broken $U(1)$ symmetry. In both models this global $U(1)$ symmetry has a QCD anomaly, and therefore $A^0$ is an axion. Note though that various axion searches place a lower bound on $M_A$, typically in the MeV range, which requires explicit $U(1)$ breaking beyond the QCD anomaly, so that $A^0$ does not solve the strong CP problem. In other models, such as the chiral supersymmetric models, or composite Higgs models from extra dimensions, $h^0$ could also decay into light CP-even scalars.

In this Letter we study the Higgs boson decay into CP-odd scalar pairs at the upgraded Tevatron. We assume the existence of a scalar $A^0$ (we call it “axion” for short), of mass $M_A < M_h/2$, with a trilinear coupling

$$\frac{e v}{2} h^0 A^0 A^0,$$

where $v \approx 246$ GeV is the electroweak symmetry breaking scale, and $c$ is a model-dependent dimensionless parameter, which can be as large as $O(1)$.

The Higgs width into a pair of axions is

$$\Gamma(h^0 \to A^0 A^0) = \frac{e^2 v^2}{32\pi M_h} \left(1 - \frac{M_A^2}{M_h^2}\right)^{1/2}.$$ (2)

The decay to axion pairs can be essential for Higgs boson searches in collider experiments. This is illustrated in Fig. 1, where we plot the Higgs boson branching ratio to axions, $B(h^0 \to A^0 A^0)$, versus $M_h$, for $M_A \ll M_h/2$ and several values of $c$. For $M_h$ below the $WW$ threshold, the dominant SM decay of the Higgs boson $h^0 \to bb$ has a very small width, and is therefore susceptible to the presence of new physics beyond the SM, e.g. the interaction $\Phi \Phi \Phi$. The decay to axions would then dominate over $h \to bb$ for values of $c$ as small as $\sim 0.02(M_h/100$ GeV). We also see that even above the $WW$ threshold, $h^0 \to A^0 A^0$ competes with $h^0 \to WW$, provided $c \sim O(1)$.
Experimental signatures of the Higgs boson.— The final state signatures for \( h^0 \to A^0 A^0 \) searches will depend on the subsequent decays of the axions, which are quite model-dependent. Here we will concentrate on the case where the axion couplings to light fermions are negligible. Such a situation may arise in the MCHM, e.g., when only one Higgs doublet is mainly responsible for electroweak symmetry breaking and fermion masses (type I two-Higgs-doublet model with large \( \tan \beta \)). In the MCHM, however, the axion has a large coupling to a heavy vector-like quark, \( \chi \), whose charges under the SM gauge group are the same as for the right-handed top quark \( t_R \). This coupling allows one-loop decays of the axion into gluon or photon pairs. The case where the axion couplings to light fermions are significant (e.g., in the NMSSM) provides interesting experimental signatures as well, but we leave its investigation for future studies.

The constraints on a light CP-odd scalar with small couplings to SM fermions are loose \([3]\). For example, no constraints on the axion mass have been set from \( Z \to A^0 \gamma \) at LEP \([10]\), from direct \( A^0 \) production through gluon fusion via a \( \chi \) loop at the Tevatron \([11]\), from fits to the electroweak data, or from meson decays \([3]\). The relevant lower bounds on \( M_A \) come from beam dump experiments \([12]\), in the MeV range, and from star cooling rates, \( M_A \gtrsim 0.2 \text{ MeV} \) \([12]\).

In the MCHM, the two Higgs doublets and two gauge-singlet scalars arise as bound states of the top-bottom left-handed doublet or \( \chi_L \), with \( \chi_R \) or \( t_R \). At scales below a few TeV this is an explicit, renormalizable theory with scalars that appear to be fundamental. The Higgs potential has been analyzed in detail in \([12,13]\). For the purpose of studying Higgs boson decays in the MCHM it is however sufficient to introduce the following simpler model. Consider the SM with the addition of a gauge singlet complex scalar \( S \) and the vector-like quark, \( \chi \). Besides the kinetic terms and Higgs Yukawa couplings, the following terms are present in the Lagrangian:

\[
\mathcal{L} = \xi S \nabla_L \chi_R + \text{h.c.} - V(H,S) ,
\]

where \( \xi \) is a Yukawa coupling, and the scalar potential is

\[
V(H,S) = \frac{\lambda_H}{2} (H^\dagger H)^2 + \frac{\lambda_S}{2} (S^\dagger S)^2 + \lambda_0 H^\dagger H S^\dagger S + M_R^2 H^\dagger H + M_S^2 S^\dagger S + C_S (S + S^\dagger) .
\]  

We assume \( M_R^2 < 0 \), and \( \lambda_H \lambda_0 > \lambda_S^2 \). In the limit where the coefficient \( C_S \) of the tadpole term vanishes, the effective potential has a global \( U(1) \) symmetry spontaneously broken by the vacuum expectation value \( \langle S \rangle \) of \( S \). The associated axion, \( A^0 \), is part of the singlet \( S \), and due to the tadpole term has a mass given by \( \sqrt{|C_S|/\langle S \rangle} \). Note that in the MCHM the tadpole term is generated by a tree level \( \chi \) mass, and there is mixing between \( \chi \) and \( t \) once the electroweak symmetry is broken. These details are not relevant for the present study, but the coupling of the axion to \( \chi \) is essential since otherwise the axion would be stable and the Higgs boson would decay invisibly \([3]\).

The \( h^0 A^0 A^0 \) coupling may be easily computed in the SM+singlet model, with the result

\[
c = -\sqrt{2} \lambda_0 S \frac{\langle S \rangle}{v} \sin \theta - \lambda_0 \cos \theta ,
\]

where \( \theta \) is the mixing angle between the two CP-even neutral scalars,

\[
\tan 2\theta \simeq \frac{-2\sqrt{2} \lambda_0 v \langle S \rangle}{2 \lambda_0 \langle S \rangle v^2 - C_S / \langle S \rangle} .
\]

For a range of values of the six parameters from Eq. \([3]\), the Higgs decay to axions is important.

The effective axion couplings to gluons and photons, induced at one-loop by the \( \chi \) quark, are given by

\[
\frac{-\sqrt{7}}{16\pi} A^0 \epsilon_{\mu
u\rho\sigma} \left( \alpha_s G_{\mu\nu} G_{\rho\sigma} + N_c \epsilon_\chi^2 \alpha F_{\mu\nu} F_{\rho\sigma} \right) ,
\]

where \( \alpha_s \) (\( \alpha \)) is the strong (fine structure) constant, \( G_{\mu\nu} \) (\( F_{\mu\nu} \)) is the gluon (photon) field strength, \( N_c = 3 \) is the number of colors and \( \epsilon_\chi = 2/3 \) is the electric charge of the vector-like quark. Naive, the dominant axion decay mode is to a pair of gluons. However, the gluons must then hadronize, and for light axions the number of open channels is very limited. Indeed, the two-body decays \( A^0 \to \pi\pi, \pi^0 \gamma \) are forbidden by CP invariance and angular momentum conservation, while the three body decays \( A^0 \to \pi^0 \gamma \gamma, 2\pi^0 \gamma, \pi^+ \pi^- \gamma \) are significantly suppressed by phase space (note that C- and P-parity need not be separately conserved in axion decays). Therefore, for \( M_A \lesssim 3 m_\pi \approx 405 \text{ MeV} \) the branching ratio to two photons is close to 1. The axion decay width due to the two photon effective coupling \([3]\) is given by

\[
\Gamma(A^0 \to \gamma\gamma) \simeq \frac{\alpha^2 M_A^3}{12 \pi^3 \langle S \rangle^2} .
\]

For \( M_A \gtrsim 0.5 \text{ GeV} \) the isospin-violating decay modes \( A^0 \to 3\pi \) open up and start to compete with \( A^0 \to \gamma\gamma \). Due to QCD uncertainties, it is quite difficult to estimate their exact width, but recall that the measured branching fractions of \( \eta \) decays into \( \gamma\gamma, 3\pi^0, \pi^+ \pi^- \pi^0 \) are given by 39\%, 32\%, and 23\%, respectively \([3]\). Since \( \eta \) and \( A^0 \) have the same quantum numbers, the \( A^0 \to \gamma\gamma \) decay mode is likely to be significant even for \( M_A \) of order 1 GeV. Fortunately, the study of the \( h^0 \to A^0 A^0 \) decay in this \( M_A \) range does not require a precise determination of the axion branching ratios, as we explain below.

The Higgs decays are quite peculiar in the scenario discussed here. Since the LEP \([12]\) and Tevatron \([13]\) limits would generally apply, we only consider the range of Higgs masses above \( \sim 100 \text{ GeV} \). Because of the relatively heavy parent mass, each axion will be produced with a significant boost, and will decay into a pair of
almost colinear photons. For \( M_A \lesssim 0.025 M_h \), they will not be resolved in the electromagnetic calorimeter and will be reconstructed as a single photon. As a result, the \( h \to A^0 A^0 \to 4\gamma \) mode will appear in the detector as a diphoton signature, as shown in Fig. 2.

\[
\begin{align*}
\gamma & \rightarrow A^0 A^0 \rightarrow h^0 A^0 \rightarrow \gamma \\
\gamma & \rightarrow A^0 A^0 \rightarrow h^0 A^0 \rightarrow \gamma
\end{align*}
\]

\( (a) \)

\[
\begin{align*}
\gamma & \rightarrow A^0 A^0 \rightarrow h^0 A^0 \rightarrow 3\pi^0 A^0 \rightarrow \gamma \\
\gamma & \rightarrow A^0 A^0 \rightarrow h^0 A^0 \rightarrow 3\pi^0 A^0 \rightarrow \gamma
\end{align*}
\]

\( (b) \)

FIG. 2. Higgs boson decay topology into a “diphoton” final state with (a) prompt and (b) cascade photons.

The interesting twist is that the \( A^0 \rightarrow 3\pi^0 \) decay mode will have the same signature in the detector, because \( \pi^0 \)'s decay promptly into photons. This situation is illustrated in Fig. 2. We can continue this line of argument for even higher \( M_A \). If \( M_A \gtrsim 1 \) GeV, the \( \omega \gamma \), \( \rho \gamma \), and \( \pi\eta\pi \) axion decay modes become relevant. Using the measured branching fractions of \( \pi^0 \) into these states, and the subsequent \( \eta', \rho, \omega \) decays, we find that the \( \eta' \) branching fraction for final states with only photons is roughly 17\%. Given the similarities between \( \eta' \) and the axion, we expect the probability that \( A^0 \) is reconstructed as a photon is of order 20\% when \( M_A \approx 1 \) GeV.

For \( M_A \gtrsim 2 \) GeV, new isospin-conserving modes with large branching fractions open up: \( A^0 \rightarrow \rho \rho, \omega \omega, a_0 \pi^0, \pi K \pi^0, \) etc. (isospin-violating decays, such as \( \eta \eta \pi \), are suppressed.) Even then, some of these mesons have large branching fractions into states which subsequently decay into photons, e.g., \( a_0 \rightarrow \eta \eta \pi^0 \), yielding the same diphoton signature for \( h^0 \). Only when \( M_A \) is increased above several GeV do the decay products of \( h^0 \) look more like QCD jets instead of photons.

An important issue is whether the \( A^0 \) decays promptly. Using Eq. 6, we can estimate its decay length

\[
L_A \approx 4 \text{ mm} \frac{M_h(S)^2}{(100 \text{ GeV})^3} \left( \frac{1 \text{ GeV}}{M_A} \right)^4.
\]

(9)

For \( M_A \lesssim 100 \) MeV the axion decays occur most of the time outside the detector, so the Higgs boson decay is invisible. In the following we shall instead concentrate on the mass range \( M_A \gtrsim 200 \) MeV, where the axion decays before reaching the electromagnetic calorimeter.

**Tevatron reach for light axions.**— For \( M_A \) less than a few GeV, we have studied the Tevatron reach in the diphoton channel, following the analysis of Ref. 17. We used PYTHIA for event generation and SHW with minor modifications for detector simulation. The Higgs boson is produced predominantly via gluon fusion, and the inclusive diphoton channel (with an optimized cut on the invariant diphoton mass, \( m_{\gamma\gamma} \)) provides the best sensitivity. The reach is shown in Fig. 3, where we plot the product \( L \times P^2(A \to \gamma) \) as a function of \( M_h \). Here \( L \) is the total integrated luminosity required for a 95\% confidence level (C.L.) exclusion, and \( P(A \to \gamma) \) is the \((M_A\)-dependent\) probability that an axion is reconstructed as a photon, including the branching fractions of cascade decays of axions into multi-photon final states. We see that already run IIa with 2 fb\(^{-1}\) will be probing a range of Higgs boson masses well beyond the reach via conventional SM searches 2. Note the reversed ordering of the lines of constant \( c \) at low and high \( M_h \). Below the WW-threshold, the Higgs boson width, \( \Gamma_h \), is dominated by the decay \( (2) \) into axions, hence a larger \( c \) requires a softer \( m_{\gamma\gamma} \) cut and leads to higher background. Above the WW-threshold, where \( \Gamma_h \) is dominated by the SM decays, a larger \( c \) is beneficial due to the increased \( B(h \to A^0 A^0) \) (see Fig. 3).

![FIG. 3. The Tevatron reach at 95\% C.L. in the inclusive diphoton channel (solid) and \( \ell\gamma\ell\gamma \) channel (dashed), as a function of \( M_h \), for three different values of \( c \).](image)

For light axions, associated \( Wh/Zh \) production can give alternative, very clean signatures: \( \ell\gamma\ell\gamma \) and \( \ell^+\ell^-\gamma\gamma \). Considering only leptonic decays of the \( W/Z \), we expect \( Wh \) to give a better reach, because of the larger leptonic branching fraction. Requiring events with \( E_{\ell} > 20 \) GeV, at least one lepton with \( p_T(\ell) > 20 \) GeV, and at least two photons with \( p_T(\gamma) > 20 \) GeV and \( |m_{\gamma\gamma} - M_h| < \Gamma_h \), we find the following parametrization of the signal efficiency:

\[
\varepsilon = 0.32 - 0.07(M_h/100 \text{ GeV}).
\]

The main background is \( W\gamma\gamma \) and we estimated it using COMPHEP to be less than 1 event after cuts in 30 fb\(^{-1}\). The corresponding reach is shown in Fig. 3 (dashed lines). We see that although this channel gives a smaller absolute reach than the inclusive \( 2\gamma \) channel, it will still enable the Tevatron to probe Higgs masses below WW threshold, for a wide range of values of \( c \).

**Tevatron reach for heavy axions.**— If \( M_A \) is above a few GeV, the decay products from \( A \to gg \) look like QCD jets, and the background is large. To make mat-
ters worse, at the parton level $A^0 \to gg$ dominates over
$A^0 \to \gamma \gamma$ by a factor of $(N_c^2 - 1)\alpha_s^2/(4N_c^2\alpha_s^2\epsilon_1^3) \approx 265$.
Typically, for $M_A \gtrsim 20$ GeV, the resulting two gluon jets are
separated well enough and can both be individually
reconstructed. Unlike the SM, the final states from Higgs
production contain no $b$-jets, but instead mostly gluon
jets and very rarely photons. Since at present it is prac-
tically impossible to distinguish between gluon and quark
jets, these searches appear quite challenging.

Gluon fusion ($gg \to A^0A^0$) can lead to $4j$, $2j2\gamma$ or
$4\gamma$ events. The $4j$ channel suffers from insurmountable
backgrounds, while the $4\gamma$ channel has a tiny branching
ratio, and will escape detection even in run IIb with 30
fb$^{-1}$. The $2j2\gamma$ channel is similar to the searches for a
“bosonic Higgs” at the Tevatron $^{15,17,22}$. Using the
same cuts as for the inclusive $\gamma\gamma + N$jets channels of
Ref. $^{17}$, we found no reach in run IIb.

Searches for associated Higgs boson production also
appear very difficult. The 6-jet final states from all-
hadronic decays of the $W$ ($Z$) and $A^0$ have large QCD
backgrounds. Leptonic decays of the $W$ and $Z$, combined
with $h \to 4j$ give $\ell\ell jE_T$ and $\ell^+\ell^-4j$, respectively. The
backgrounds are large and again no sensitivity in run II is
expected. Finally, requiring that one axion decays to
$\gamma\gamma$, and leptonic decays of the $W$ or $Z$, we get the relatively
clean $2\gamma jE_T + X$ and $\ell^+\ell^-2\gamma + X$ final states. Because
of the $B(A^0 \to \gamma\gamma)$ suppression, the signal rates are too
small to be observed in run IIa, but run IIb might be
able to explore the mass range $100 \lesssim M_h \lesssim 120$ GeV.

**Discovery prospects at the LHC and future lepton colliders.**— It is interesting to contemplate the capabilities
of future colliders for our scenario. The LHC has
effortless potential for such Higgs boson searches. Just
like at the Tevatron, one will have to concentrate on the
cleanest channels. But the much larger signal rate will
allow one to look for the photonic decays of heavy axions,
which were severely limited by statistics at the Tevatron.

Preliminary studies show that even the $2j2\gamma$ channel,
swamped by the QCD background at the Tevatron, is
sensitive to a large range of Higgs boson and axion masses
at the LHC, due to the improved energy resolution of the
LHC detectors and the enhanced signal cross section.

A high energy lepton collider (such as the NLC) would
be ideally suited for unravelling a non-standard Higgs
sector, like the one discussed in this Letter, particularly if
$M_A$ is bigger than a few GeV and $P(A \to \gamma)$ is very small.
Notice that the jet-rich channels are the best to look for
at a lepton collider, since they have the largest branching
ratios. In this sense, lepton colliders are complementary
to hadron machines, where these channels suffer from
large backgrounds. We also expect that LEP-II will be
able to probe Higgs masses up to its kinematic reach,
onece a dedicated search is done. We therefore urge the
LEP collaborations to present Higgs mass limits with
the data selection optimized for the discussed signatures.

In conclusion, we have considered several novel Higgs
boson discovery signatures, arising from the decay $h^0 \to
A^0A^0$, present in many extended Higgs sector models.
Quite ironically, the best reach at the Tevatron is
obtained for light axions, where the Higgs boson often
decays to two jets, each of which “fakes” a photon.

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