Recycling of vitrimer blends with tunable thermomechanical properties†

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Vitrimers are a new class of thermosetting polymers that can be thermally processed through bond exchange reactions (BERs) without losing network integrity. In engineering applications, the tunability of their thermomechanical properties is highly desirable to meet the requirements of different working conditions. Here, we report a simple composite-based strategy that avoids complex chemistry to prepare vitrimer blends with tunable thermomechanical properties by virtue of the good weldability of base vitrimers. Effects of processing parameters (such as temperature and time) on the properties of recycled vitrimer blends are experimentally investigated. A computational model that accounts for the random distribution of component vitrimer particles is developed to predict the thermomechanical properties of the recycled vitrimer blends with various compositions. Good agreement is achieved between theoretical prediction and experiment. Parametric studies are further conducted by employing the computational model to explore the designability and provide some basic principles to guide the design of recycled vitrimer blends. Reasonable recyclability of the vitrimer blends is verified by multiple generations of recycling experiments.

1 Introduction

Thermosetting polymers crosslinked by covalent bonds (epoxy,phenolic,bismaleimide and cyanate ester resins, etc.) are capable of maintaining their integrity upon heating, and thus possess excellent properties including superior chemical resistance, and stable thermal and mechanical properties at high temperatures, which make them ideal choices in a variety of engineering fields ranging from electronics and aerospace to the automotive industry. However, the chemically cross-linked nature brings considerable difficulty in reprocessing and recycling such materials, giving rise to increasing economic and environmental concerns.

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Recently, a new class of thermosetting polymers, known as vitrimers, which can be thermally processed without losing network integrity through bond exchange reactions (BERs), has changed the traditional view of thermosetting polymers. Vitrimers behave like traditional thermosets at room temperature, while tend to be reshapable, reprocessable, and recyclable at elevated temperatures due to the inherent dynamic covalent bonds (DCBs). These innovative features possessed by vitrimers expand the lifetime and potential applications of thermosetting polymers. Since Leibler and coworkers first introduced the name vitrimers for the epoxy networks which were developed based on transesterification reaction in 2011, several alternative chemistries have been explored.

The tunability of the thermomechanical properties of the vitrimers is highly desirable in engineering applications to meet the requirements of different working conditions. For instance, when an epoxy-based vitrimer is used as a structural material, we normally expect to increase its modulus at room temperature to meet the requirement of load-bearing capacity; on the other hand, decreasing its rubbery modulus eases the reprocessing at high temperature. However, for the existing chemistry-based methods, such as adjusting the stoichiometry of monomers or choosing different monomers, increasing room-temperature modulus and decreasing rubbery modulus of vitrimers are mutually exclusive since the cross-linking density or the rigidity of the entire network is tuned. Therefore, it is necessary to further explore other methods to expand the tunability of the thermomechanical properties of vitrimers.
Furthermore, since vitrimers possess the virtue of recyclability, from both environmental and economic points of view, it is valuable that new vitrimers with different mechanical performances can be fabricated by reprocessing the “waste” vitrimers, rather than involving complex chemistry.

In this work, we report a composite-based strategy to prepare vitrimer blends with tunable thermomechanical properties utilizing the good weldability of vitrimers. Two different transesterification-based epoxy vitrimers were respectively synthesized by reactions of diglycidyl ether of bisphenol A (DGEBA) with fatty acids and glutaric anhydride, showing different thermomechanical properties.\textsuperscript{11} The resulting vitrimers were pulverized into powders followed by being mixed at different ratios to prepare vitrimer blends under reprocessing conditions. The transesterification-based property of both base vitamers facilitates the interfacial welding of mixed vitrimer particles. Dynamic mechanical analysis (DMA) and uniaxial tensile test were carried out to investigate the effect of processing parameters (such as temperature and treating time) on the thermomechanical properties of recycled vitrimer blends. By simply varying the composition of the two base vitrimers in their pulverous states, the thermomechanical properties of the recycled vitrimer blends were tuned within the limits regulated by the pure base vitrimers. To better understand the operative phenomena and assist the design of vitrimer blends, a computational model accounting for the random distribution of component vitrimer particles was developed. Parametric studies were further conducted by employing the model to explore the designability of the vitrimer blends. In addition, recyclability of the vitrimer blends was investigated through multiple generations of recycling experiments.

2 Experimental

2.1 Material synthesis

Two epoxy-based vitrimers were synthesized according to the reported procedures (Fig. S1†),\textsuperscript{11,12} where monomers with different chain lengths were used to generate their distinction in crosslinking density. Accordingly, these two vitrimers have different glass transition temperatures ($T_g$) and room-temperature modulus, which were regarded as soft and hard networks. But both of them ran transesterification at elevated temperature. Details regarding the synthetization can be found in the ESI.†

2.2 Preparation of powders

Bulk samples of the two aforementioned pure vitrimers were respectively grinded into powders by using a variable speed rotor mill branded PULVERISSETTE 14 (Fritsch, Germany) equipped with a trapezoidal perforation sieve with ring size of 0.5 mm. The grinded particles were then transferred to a digital microscope (Hirox, Japan) for morphology observation.

2.3 Preparation of recycled samples

Vitrimer powders were prepared by first mixing the two types of powders in different weight ratios followed by pouring the powder mix into a customized aluminum mold. Then we pre-heated the CARVER press (Model 4386, USA) machine to the target temperature and transferred the mold into the machine chamber where the mixed powders were hot-pressed for a set time under constant pressure.

2.4 Dynamic mechanical analysis

Dynamic mechanical analysis (DMA) tester (Q800, TA Instruments, New Castle, DE, USA) was used to characterize the thermomechanical properties of the vitrimer blend samples in the tension mode. Samples with the dimension of 15 mm × 5 mm × 0.5 mm were tested at a frequency of 1 Hz with a peak-to-peak amplitude of 2%. The temperature was first equilibrated at −50 °C for 5 min, and then gradually increased to 120 °C at a rate of 2 °C min$^{-1}$. The glass transition temperature ($T_g$) was identified as the temperature corresponding to the peak of loss factor (tan δ) curve.

2.5 Uniaxial tension tests

For the room-temperature uniaxial tension tests, the universal material test machine Instron (Model 5943, Germany) was used in the displacement-controlled mode with a load cell of 1 kN. Samples with the dimension of 15 mm × 5 mm × 0.5 mm were tested at a loading rate of 5% min$^{-1}$ to minimize viscoelastic effects. For each case, three samples were tested, and the average value was reported. For the tests at high temperature (100 °C), the DMA tester was used where the loading rate and sample dimension were the same as the tests performed at room temperature.

3 Computational modeling

To predict the thermomechanical properties of the recycled vitrimer blends with various compositions, a computational model was developed where the temperature-dependent thermomechanical behaviors of the pure vitrimers and the random distribution of the component vitrimer particles within the blends were both taken into account.

3.1 Thermoviscoelastic model for the pure vitrimer

For the pure vitrimers with hard or soft network, a multibranch thermoviscoelastic model was employed where one equilibrium branch and several thermoviscoelastic nonequilibrium branches were arranged in parallel (Fig. 1a).\textsuperscript{33,34} More details can be seen in the ESI.†

3.2 Finite element computational model

Finite element (FE) simulations of the DMA test for the pure vitrimers were conducted to validate the accuracy of the above characterized material parameters by using the commercial software package ABAQUS (Dassault Systems, Johnston, RI, USA). A two-dimensional square representative volume element (RVE) constrained by periodic boundary conditions was built and assigned with the properties of pure vitrimer. The aforementioned multibranch thermoviscoelastic constitutive
relations was programmed in the FE simulations by importing the fitted viscoelastic parameters (given in Table S1†) into the time-domain Prony-series provided in ABAQUS material library together with a UTRS subroutine to define the time-temperature superposition (TTSP) relationship. Four-node bilinear plane stress elements (ABAQUS element type CPS4) were employed to mesh the entire part. Dynamic, implicit analyses were conducted at elevated temperatures under a uniaxial sinusoidal oscillation strain at a frequency of 1 Hz with a peak-to-peak amplitude of 2%. The calculated phase lag between the stress and strain curves determines the loss factor (tan δ) while the storage modulus is taken to be the quotient of the stress and strain amplitudes. It is seen from Fig. S2 (FE simulation part in ESI†) that good agreement is achieved between the experiment and simulation of the storage modulus and tan δ of the vitrimer blends with various composition (7 : 3, 5 : 5 and 3 : 7) were predicted and the comparison between the experiment and simulation are shown in Fig. 4a and b.

4 Results and discussion

4.1 Characterization of the polymer particles

As the microscopic images shown in Fig. 2a and c, the particles grinded from soft and hard networks are both in irregular shapes with different sizes.

To further obtain the particle size distributions of the grinded powders from different vitrimers, microscope images were analyzed by using the commercial image processing software Image J. The profiles of the particles were extracted from the microscopic image and the size of each particle was taken to be the diameter of a circle with an equal area of the corresponding particle profile. Fig. 2b and d show the particle size distributions of the grinded powders from soft network and hard network. The volume fraction of the particles with diameter ranging from 100 μm to 400 μm is calculated to be 70% for soft network and 68% for hard network, which indicates that with the same mesh size of sieve ring, there is no apparent difference in the average particle size between the soft and hard networks.

4.2 Effects of treating time and temperature

Since the transesterification reaction is time and temperature dependent,12 the effects of these two treating parameters on the
thermomechanical performances of vitrimer blends were investigated.

To explore the effect of treating time, the mixed vitrimer powders (soft : hard = 1 : 1) were thermally treated at 200 °C under a controlled pressure of 16 MPa for 20 min, 40 min, 1 h, 2 h, 4 h and 6 h, respectively. It is seen from Fig. 3a–c that the increase of heating time from 20 min to 2 h results in a gradual increase of rubbery modulus from ~4.7 MPa to ~10 MPa, which suggests that the voids in the vitrimer blends are gradually closed and more polymer chains are connected between particle interfaces.15–15 Above the heating time of 2 h, the rubbery modulus becomes heating time-independent, indicating the interfacial chain density reaches a saturated level. In addition, two different glass transition temperatures of ~28 °C and ~75 °C could be found for the vitrimer blends and the values are barely affected by the heating time. Moreover, the uniaxial tension curves of the vitrimer blends at 100 °C (Fig. 3d) shows that an improved stretchability could be obtained by the vitrimer blends with an increasing heating time from 20 min to 4 h where the break strain increases from 6.5% to 15%.

Previous work by Yu et al.15 showed that the interfacial welding of vitrimer follows the Arrhenius-type TTSP. Therefore, increasing the heating temperature shows the same effect to improve the mechanical performance of the vitrimer blends as increasing the heating time. Detailed experimental results are shown in Fig. S3 of the ESL†

Overall, time and temperature will affect the extent of bond exchange reactions at the interfaces of vitrimer particles. With the increase of time or temperature, the interfacial chain density will increase, which therefore leads to the increase of modulus. However, when the time or temperature increases to a certain extent, the interfacial chain density becomes saturated, and correspondingly the modulus maintains constant.

4.3 Effect of composition

The vitrimer blends can be regarded as a composite whose mechanical properties approximately follows the rule of mixtures. Therefore, their thermomechanical properties could be tuned by simply varying the mixing ratio between the two base vitrimer. The temperature dependent storage modulus and tan δ of the vitrimer blends with varying composition are respectively shown in Fig. 4a and b, and the corresponding rubbery modulus and glass transition temperatures (Tgs) are summarized in Fig. 4c. Simulation results obtained by the computational model are observed to agree well with the experiment results, which validates the accuracy of the developed model. It is seen from Fig. 4c that the rubbery modulus gradually increases from 1.1 MPa to 18 MPa with the weight ratio of hard vitrimer varying from 0% to 100%.

In addition to the DMA results, uniaxial tension results shown in Fig. 4d and e further show the tunability of the stiffness and stretchability by varying the blend composition. It is seen in Fig. 4e that as the ratio of hard vitrimer increases, the Young's modulus of the vitrimer blends gradually increases from 3 MPa to 1.15 GPa, along with the decrease of break strain from 200% to 10%.

Fig. 3 Effect of heating time on thermomechanical performance of recycled vitrimer blends. Storage modulus (a) and tan δ (b) as a function of temperature. (c) The effect of heating time on glass transition temperature and rubbery modulus. (d) Strain–stress behavior of recycled materials with 50% of hard network at 100 °C (rubbery state). All the samples were prepared by mixing 50% of soft network and 50% hard network polymer powders resulting from the utilization of 0.5 mm trapezoidal perforation sieve rings under the same controlled pressure of 16 MPa at 200 °C.

Fig. 4 Effect of composition on the thermomechanical performance of recycled vitrimer blends. Storage modulus (a) and tan δ (b) as a function of temperature. Solid lines illustrate experimental results and dash lines denote the prediction by using the computational model. (c) The effect of composition on glass transition temperature and rubbery modulus. (d) Strain–stress behavior of vitrimer blends at room temperature. S: soft; H: hard. (e) The effect of composition on Young's modulus and break strain. All the samples were prepared by mixing polymer powders resulting from the utilization of 0.5 mm trapezoidal perforation sieve rings under the same controlled pressure of 16 MPa at 200 °C for 2 h.
At this point, it should be noted that it is valuable that new vitrimer blends with tunable thermomechanical properties can be generated by simply mixing the existing “waste” pure vitrimer powders without involving complex chemistry. Such simple method is eco-friendly and enables us to meet the requirement of different working conditions for practical engineering applications.

4.4 Designability of the vitrimer blends

Since the material combination used in the actual experiment is limited and the accuracy of the computational model has been validated, parametric studies could be conducted by using the model to further explore the designability of the vitrimer blends. In this sub-section, two design examples are studied where the rubbery modulus, glass transition temperature difference, and $\tan \delta$ breadth of the base vitrimers are designing parameters.

The first design example shown in Fig. 5 explores the possibility of decreasing the rubbery modulus of the vitrimer blends while enhancing their modulus at room temperature. Normally, we want a vitrimer possesses a high modulus at low temperature to meet the requirement of load-bearing capacity as a structural material. Also, a lower rubbery modulus is expected to meet the requirement of reprocessing under a low pressure. As shown in Fig. 5a and b, we create the base material 2 in the computational model to be the vitrimer to be modified, and the base material 1 is the modifier vitrimer with a lower rubbery modulus and higher glass transition temperature. The simulation results of the temperature-dependent storage modulus of the vitrimer blends are shown in Fig. 5c, and the corresponding values at room temperature (25 °C) and high temperature (105 °C) are respectively recorded in Fig. 5d. It is seen that the room-temperature modulus of the blends increases linearly in the logarithm scale with the weight ratio of base material 1, while the rubbery modulus at 105 °C linearly decreases, confirming the feasibility of tuning the material stiffness as designed.

The second example shows the possibility of tuning the miscibility of the vitrimer blends. For the completely miscible blends, only one glass transition can be observed in the DMA curves with a single $T_g$ lying between the $T_g$s of base components. As shown in Fig. 4a and b, there are two peaks in each $\tan \delta$ curve and one plateau in each storage modulus curve for the vitrimer blends created in the actual experiments, which indicates that the two base vitrimer components of the blends are not completely miscible. It is intriguing to explore if it is possible to modify the miscibility by decreasing the glass transition temperature difference and broadening the $\tan \delta$ breadth of the base vitrimer materials. As shown in Fig. 6a and b, two base vitrimers (base material 3 and 4) with close glass transition temperature and broad transition region are designed. The simulation results of the temperature-dependent storage modulus and $\tan \delta$ curves of the vitrimer blends are respectively shown in Fig. 6c and d. It is seen that upon mixing, there are no plateau in the storage modulus curve and only one peak in the $\tan \delta$ curve, which meets the goal of our design.

4.5 Recyclability of the vitrimer blends

Since the covalent bonds of vitrimer blends are only exchangeable but not consumed during thermal processing, the resulting blends have the potential to be recycled for several times.

Fig. 7a compares the storage modulus curves for the 1st and 3rd generation of the recycled vitrimer blends obtained from the experiments. During each reprocessing cycle, the samples were
thermally treated at 200 °C under a controlled pressure of 16 MPa for 2 h. The curves nearly overlapped with each other, except that the rubbery modulus was slightly decreased from 8.5 MPa to 7.3 MPa. The decrease of rubbery modulus might be resulted from the breakage of permanent covalent bonds during the vitrimer grinding.\(^{37}\) The glass transition temperatures show no apparent change after three reprocessing cycles (Fig. 7b). The stress-strain curves plotted in Fig. 7c illustrate that the mechanical properties of the recycled samples slightly degrade after each recycling treatment, yet compared to the 1st recycled sample, the 3rd generated sample maintains the comparable stretchability and 80% of the stiffness, showing the reasonably good recyclability.

5 Conclusion

In this work, we demonstrate a composite-based strategy to prepare vitrimer blends with tunable thermomechanical properties and reasonable recyclability by virtue of the dynamic covalent bond. Sufficient thermal processing with high processing temperature and long processing time may enhance the interface bonding, which accordingly induces higher modulus and greater stretchability. The tunable thermomechanical properties of vitrimer blends can be realized by adjusting the compositions of the base vitrimers, which offers a flexible and eco-friendly way to recycle the thermoset waste for practical engineering applications. To assist the blends design, a computational model accounting for the temperature-dependent thermomechanical behaviors of the pure vitrimers and the random distribution of the component vitrimer particles was developed to predict the thermomechanical properties of the recycled vitrimer blends. The validity of the computational model was proved by the good agreement between the experimental results and theoretical predictions of the thermomechanical properties of the recycled vitrimer blends with various compositions. The designability of the vitrimer blends was investigated by the parametric studies, showing the capability of increasing room-temperature modulus while decreasing the rubbery modulus, and generating vitrimers with good miscibility by decreasing glass transition temperature difference and broadening the tan δ curve breadth of pure base components. Finally, the reasonable recyclability of the vitrimer blends was verified. We expect that this composite-inspired blending method can be expanded to other transesterification-based vitrimers with excellent mechanical performance (high \(T_g\), stiffness and strength) to satisfy most requirements of practical applications.

Conflicts of interest

There are no conflicts to declare.

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