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ABSTRACT
Titanium dioxide (TiO\(_2\)) and especially its polymorph, anatase, are widely used transition-metal oxides for renewable energy applications such as photocatalytic and photovoltaic devices due to their chemical stability and their electrochemical and photocatalytic properties. However, the wide energy bandgap of anatase limits its photocatalytic ability and electron transport properties. Doping with appropriate elements is an established way to control and tune the optical and electronic properties of anatase such as conductivity, transparency, and bandgap. Metal doping can improve anatase’s properties as an electron transport material, whereas non-metal (anion) doping is widely used to improve its photocatalytic activity. Herein, we investigate the effect of carbon group dopants in conjunction with hydrogenation of TiO\(_2\) by applying density functional theory. We find that hydrogenation has a positive impact on the structural and electronic properties of TiO\(_2\), thus making it an appropriate candidate for energy harvesting devices.

I. INTRODUCTION
Following the systematic study of Fujishima and Honda,\(^1\) TiO\(_2\) and many other metal oxides, such as tin oxide (SnO\(_2\)), tungsten trioxide (WO\(_3\)), and aluminum trioxide (Al\(_2\)O\(_3\)), have been extensively investigated due to their interesting photocatalytic properties, high chemical stability, and long lifetime photo-generated carriers.\(^{1-16}\) Anatase TiO\(_2\) is often used as an electron transport material in organic solar cells (OSCs) and perovskite solar cells (PSCs) due to its intrinsic \(n\)-type conductivity and adequate electron mobility attributed to oxygen vacancies formed during deposition. However, anatase has a wide bandgap (3.2 eV) that limits its absorption in visible-light and near-infrared (NIR) regions.\(^{11}\) To increase the catalytic performance of anatase TiO\(_2\), many strategies have been investigated, such as formulation of ternary oxides,\(^{12,13}\) defect engineering (e.g., halogen doping\(^{14}\) and formation of oxygen vacancies), application of stresses,\(^{15}\) and introduction of disorder in the lattice.\(^{16}\) In this context, Chen \textit{et al.}\(^{16}\) engineered anatase TiO\(_2\) and, through hydrogen doping, synthesized the so-called black titania with a bandgap of 1.54 eV due to an upward shifted valence band (VB) edge by hydrogen insertion. The hydrogen concentration of their samples was 0.25 wt. \%, which corresponds to one H atom per five Ti atoms. Their results point to a strong dependence of the electronic properties on the hydrogen concentration. Through density functional theory (DFT) calculations, Liu \textit{et al.}\(^{17}\) predicted that hydrogen atoms contribute to surface disordering, by breaking Ti–O bonds and creating Ti–H and H–O pairs.\(^{17}\) Other studies suggested that the improvement in the visible-light
absorption is related to the formation of the bonds on the surface of H:TiO₂.¹⁸–²¹

Besides hydrogen, many transition-metal cations have been also used as dopants in TiO₂.²²–²⁵ However, it is expected that despite the conductivity enhancement upon doping, the enhanced photocatalytic activity of cation-doped TiO₂ might be because the dopant-related localized d-states act as recombination centers for the photogenerated carriers.²²–²⁵ Conversely, carbon dopants amplify the photocatalytic activity of TiO₂ in the visible-light region as they introduce new states inside the bandgap without acting as recombination centers.²⁶–²⁹ Doping with both C and N results in about a 50 nm red shift in the absorption spectra²⁶–²⁹ and produces photoactivity in the visible-light region. Recent results with carbon doping further demonstrate improved photocatalytic efficiency in water splitting with a total conversion efficiency of up to 11%. Gao et al.³⁰ reported that doping of TiO₂ with carbon cations present in different oxidation states influences the crystal structure, the charge density, and the optical properties compared to the pure TiO₂. However, in the literature, there are many explanations for the enhanced photocatalytic activity of C:TiO₂.³¹–³⁴

For silicon doping of TiO₂ (Si:TiO₂), Oh et al.³⁵ predicted that in small dopant concentrations, Si could improve the photocatalytic properties of TiO₂. Yan et al.³⁶ indicated that the substitutional doping of Ti with Si causes a broadening of the optical absorption. Moreover, Ozaki et al.³⁷ prepared N:Si:TiO₂ with strong absorption in the visible-light region and with high photocatalytic activity. Other dopants, such as germanium (Ge), can also reduce the bandgap of TiO₂, whereas tin (Sn) doping of TiO₂ causes a slight bandgap broadening.³⁸ From an experimental point of view, Li and Zeng³⁹ showed that in the case of Sn:TiO₂, the bandgap is reduced about 0.13 eV when Sn is inserted as a substitution for Ti in a small concentration. Xiong and Balkus⁴⁰ also predicted that the photodegradation of various dyes for Sn:TiO₂ is more effective than for P25 and the optados code was used with a denser mesh of 5 × 5 × 5 k-points. The convergence criteria for the plain TiO₂ were calculated as follows: The spectral correlation factor (SCF) tolerance was set at 2.0 · 10⁻³ eV/atom, the maximum force tolerance was calculated as 0.05 eV/Å, the maximum stress tolerance was at 0.1 GPa, and the maximum displacement tolerance was at 0.001 Å. The efficacy of this approach was discussed in the previous work.⁴¹,⁴² Related techniques can provide significant insights into the electronic structure and defect engineering strategies that can improve energy materials.⁴³–⁴⁶

III. RESULTS AND DISCUSSION

A. Structural properties

Anatase belongs to the tetragonal space group I4/amd with lattice parameters a = 3.782 Å and c = 9.502 Å.⁴⁷ We calculate the lattice parameters of the perfect cell to be a = 3.806 Å and c = 9.73 Å for the unit cell and a = 11.41 Å, c = 9.73 Å, and volume = 1267.40 Å³ for the 3 × 3 × 1 supercell. In order to examine the effect of doping on the anatase structure, we use the supercell method with a supercell of 108 atoms. The dopants (C, Si, Ge, and Sn) are examined in the Ti-substitutional position, which is more favorable energetically than the interstitial one, whereas hydrogen has been examined both as an interstitial dopant and as a substitutional dopant at O positions.

For each dopant X, we calculate the optimized geometry of the supercell with X as a substitutional dopant and then we study the effect of H on this structure, with H examined at an interstitial position or at a substitutional neighboring O position.

In this mode, for the C dopant, we examine the geometry of the cell at a (a) Ti substitutional position of non-hydrogenated anatase: C₁₀:TiO₂, (b) hydrogenated anatase with H at an interstitial position, H₃:CH₃:TiO₂, and (c) H₂O:CH₃:TiO₂, hydrogenated anatase with H at a neighboring O substitution position. In Fig. 1, we present the calculated structures, whereas their structural parameters are shown in Table I.

Substitution of Ti for C produces a minimal distortion in the lattice. The C–O distance is 2.32 Å, which is larger than the standard Ti–O distance of 1.94 Å. It is therefore concluded that carbon increases the lattice constants and the cell volume, despite its smaller ionic radius compared to Ti⁴¹, which is in agreement with experimental results. Chen et al.⁴² performed experiments on C:TiO₂ and, based on Bragg’s law, calculated that the doping of TiO₂ with carbon slightly increases the lattice constants and the cell volume. The experimental results are presented in Table I for reference. We also calculated the relaxed system of minimum energy, where hydrogen is an interstitial defect (Hᵢ). The preferred position of H at the lattice is calculated at a distance of 2.07 Å near the carbon atom. After Hᵢ co-doping, the calculated lattice volume slightly decreases compared to that in carbon doping only, but it remains larger than of pristine TiO₂. To explain the small decrease in lattice volume of C₁₀:TiO₂, we should take into account that as Hᵢ binds to O, it makes it less electronegative, and as a result, the Ti–O

II. METHODOLOGY

For the DFT calculations, the plane wave code CASTEP⁴¹,⁴² was used, with exchange–correlation interactions modeled with the Perdew-Burke-Ernzerhof (PBE)⁴³ density functional in the generalized gradient approximation (GGA) with ultrasoft pseudopotentials.⁴⁴ The cut-off energy of the wave basis was set at 480 eV, in conjunction with a 2 × 2 × 3 k-point Monkhorst–Pack⁴⁵ grid. For our calculations, a 3 × 3 × 1 repeat unit cell, which results in a 108-atomic site supercell, was used. To include the effect of localized electrons, onsite Coulomb repulsions⁴⁶ of 8.2 eV were set for the 3d orbitals of Ti.¹⁵ The calculations were under constant pressure conditions. For the DOS calculations, a denser mesh of 3 × 3 × 3 k-points was applied, whereas for the partial density of states (PDOS), the optados code was used with a denser mesh of 5 × 5 × 5 k-points. The convergence criteria for the plain TiO₂ were calculated as follows: The spectral correlation factor (SCF) tolerance was set at 2.0 · 10⁻³ eV/atom, the maximum force tolerance was calculated as 0.05 eV/Å, the maximum stress tolerance was at 0.1 GPa, and the maximum displacement tolerance was at 0.001 Å. The efficacy of this approach was discussed in the previous work.⁴¹,⁴² Related techniques can provide significant insights into the electronic structure and defect engineering strategies that can improve energy materials.⁴³–⁴⁶

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FIG. 1. Minimum energy structures in anatase: (a) C_{3Ti}, (b) H_{i:CTi:TiO2}, and (c) H_{o:CTi:TiO2}.

For the H_{o:CTi:TiO2} case, we predicted a reduction of the cell volume compared to that of C_{3Ti}:TiO2, but still, it was calculated larger than the TiO2 volume. This reduction is explained on the basis of a smaller electron density residing on the Ti atoms upon oxygen substitution with hydrogen causing a weaker Ti–Ti repulsion and decrease in the bond length between Ti cations similarly to the previous explanation. Generally, in the examined H, C co-doped systems, the optimized structures become orthorhombic (a > b), in which the cell parameters a and b are larger, while c is slightly smaller than that of anatase TiO2. The above result is in good agreement with other theoretical investigations.55

Focusing on Fig. 2, the Si-doped case is presented. In Fig. 2(a), it is seen that Si can substitute a Ti atom. The supercell parameters and volume are significantly reduced. This can be attributed to the smaller ionic radius of Si^{4+} (40 pm) compared to Ti^{4+} (61 pm). After H_{i} and H_{o} doping, the lattice constants were slightly increased, but again, they are smaller than those of the pure TiO2. Similar works on Si:TiO2 have also predicted a lattice volume reduction upon Si doping.56,57

The H:Ge:TiO2 case is presented in Fig. 3. First, it is calculated that Ge_{1} doping does not affect the lattice constants and the volume. This is because the ionic radius of Ge^{4+} (53 pm) is relatively close to that of Ti^{4+}.68 Our results agree with the results of experiments performed by Chatterjee and Chatterjee.68 Specifically, it was predicted that the lattice constant along the c axis decreases with the increase in the germanium concentration, while the a constant is seen to remain the same. After H_{i} and H_{o} incorporation, the lattice constants and the volume are slightly increased.
FIG. 2. Minimum energy structures in anatase: (a) Si$_{13}$Ti$_2$H$_2$O$_2$, (b) Si$_{13}$Ti$_2$H$_2$O$_2$, and (c) H$_2$Si$_{13}$Ti$_2$O$_2$. 

FIG. 3. Minimum energy structures in anatase: (a) Ge$_{13}$Ti$_2$H$_2$O$_2$, (b) Ge$_{13}$Ti$_2$H$_2$O$_2$, and (c) H$_2$Ge$_{13}$Ti$_2$O$_2$. The germanium atom is in silver color, while hydrogen is in pink color.
FIG. 4. Minimum energy structures in anatase: (a) \( \text{Ge}_r \) Ti, (b) \( \text{H}_r \text{Ge}_r \) TiO_2, and (c) \( \text{H}_2 \text{Ge}_r \) TiO_2. The tin atom is in orchid color, while hydrogen is in pink color.

FIG. 5. Densities of states for (a) pure, (b) C Ti doped, (c) \( \text{H}_r \text{C}_r \) doped, and (d) \( \text{H}_2 \text{C}_r \) doped TiO_2.
Last, we examined H:Sn:TiO$_2$ (Fig. 4). We predicted that the lattice constants and the volume of Sn$_x$TiO$_2$ do not change significantly despite the larger ionic radius of Sn$^{4+}$ (71 pm) compared to Ti$^{4+}$. In their experimental investigation, Duan et al. also concluded that the anatase crystal structure is not significantly influenced by Sn doping. However, the dopant concentration was found to play an important role in varying the lattice constants. In this case, hydrogen doping slightly increases the lattice constants. All the above structural results are presented in Table I. It is seen that only in the Si:TiO$_2$ and H:Si:TiO$_2$ cases, the supercell is reduced.

### B. Electronic properties

The total density of states of the energetically minimum sites of the defects is considered in order for the electrical properties to be investigated. The present calculations were performed with the Hubbard $+U$ model with $U = 8.2$ eV. The calculated bandgap was 3.14 eV, in excellent agreement with the experimental value (3.2 eV). We present the total DOS of the pure TiO$_2$ in Fig. 5(a) for reference, and in Table II, we include the bandgap values for the doped TiO$_2$. As we show in Fig. 5(b), C$_{Ti}$:TiO$_2$ has a DOS very similar in shape to that of the pure TiO$_2$. It is seen that with substitutional carbon doping, the bandgap is calculated as 2.95 eV, in good agreement with other theoretical predictions. From an experimental point of view, it is seen that the bandgap of C:TiO$_2$ reaches a value of 2.97 eV, which is in good agreement with our results.

Focusing on the optical properties of C:TiO$_2$, the UV-Vis experiments showed that a noticeable shift of the absorption edge to the visible-light region is observed and this can be attributed to the predicted bandgap reduction. For the hydrogenated structure having additional interstitial H$_i$, the bandgap is further reduced to 2.80 eV [Fig. 5(c)], while with H as O-substitutional, the bandgap reaches a value of 2.85 eV [Fig. 5(d)]. In Fig. 6, the pDOS is presented. In Fig. 6(b), it is seen that the valence band is mainly created from the O-2p states, whereas the conduction band is created from Ti-3d.

When H is in the interstitial position, the calculations predict the creation of the gap states near the mid-gap and near the conduction band. The latter are very close to the conduction band minimum, hence constituting acceptor states for the co-doped oxide. In Fig. 6(c), it is seen that the gap states are created from hybridization of Ti-3d with O-2p and H-2s. In the case of H$_i$:C$_{Ti}$:TiO$_2$, again, mid-gap states are created. This implies that H$_i$:C$_{Ti}$:TiO$_2$ behaves as an electron acceptor, which is very important for its function as either a photocatalyst or an electron transport material, as these states are created near the valence band [Fig. 6(d)].

### Table II. Bandgap values for the X ($=$ C, Si, Ge, Sn) doped TiO$_2$.

| Dopant | TiO$_2$ (eV) | H$_i$:TiO$_2$ (eV) | H$_o$:TiO$_2$ (eV) |
|--------|--------------|-------------------|-------------------|
| C      | 2.95         | 2.79              | 2.85              |
| Si     | 2.90         | 2.85              | 2.70              |
| Ge     | 2.98         | 2.80              | 2.85              |
| Sn     | 3.0          | 2.75              | 2.88              |

![Fig. 6](https://example.com/fig6.png)
These states are created due to the hybridization of C-2p states with H-1s states as was described in the literature. Notably, the mixing of O-2p states that mainly contribute to the VB with C-2p orbitals leads to an upward shift of the VB edge, hence resulting in the bandgap reduction. This reduction indicates that the photocatalytic ability of C:TiO₂ in the visible-light region might be due to the contribution of C-2p states to the VB maximum, while for the co-doped case, a higher photocatalytic activity is expected due to further bandgap narrowing upon the insertion of H within the crystal.

When TiO₂ is doped with Si Ti, the bandgap is reduced to 2.90 eV, and this type of doping also creates some available states near the conduction band [Fig. 7(a)]. This result is in good agreement with that of the theoretical investigation of Lin et al. who calculated a bandgap of 2.9 eV. The experiments regarding Si:TiO₂ predicted a significant reduction of the bandgap of nearly 0.32 eV upon silicon incorporation, which is in close agreement with the reduction predicted herein. From the pDOS in Fig. 8(a), it is seen that the silicon 3p states mainly contribute to the valence band. When we dope SiTi:TiO₂ with H, we calculated that the bandgap is slightly reduced to 2.85 eV, with mid-gap states appearing at 1.95 eV. From the PDOS in Fig. 8(b), it is seen that these states are mainly attributed to the hybridization of Ti-3d with O-2p and H-2s orbitals. On the other hand, when hydrogen is an O-substitutional dopant, the bandgap is further reduced to 2.70 eV [Figs. 9(b) and 10(b)]. In this case, mid-gap states are calculated at 1.80 eV and available gap states at 2.72 eV. From all the above, it is expected that Ho:SiTi:TiO₂ also behaves as an acceptor (n-type semiconductor).

Continuing with the Ge Ti:TiO₂ case, it is shown in Figs. 9(a) and 10(a) that the bandgap is reduced to 2.98 eV with Ge atoms contributing to the valance band. This is in good agreement with the study of Chang et al. who calculated a bandgap of ~3 eV. The optical bandgap of Ge:TiO₂ was computed from UV-Vis experiments as 3 eV, which is again in good agreement with our results. It was predicted that the substitutional dopants alter the electronic structure and the photon absorption efficiency of TiO₂ and induce an electronic coupling effect with the TiO₂ atoms. After hydrogen doping, the bandgap reached a value of 2.80 eV and 2.85 eV for H [Figs. 9(b) and 10(b)] and H0 [Figs. 9(c) and 10(c)], respectively. In both cases, mid-gap states are created. Those states are favorable paths for electron transport, hence improving the electron transport capability of the oxide while the bandgap reduction increases its light absorption efficiency.

Finally, for the SnTi:TiO₂ (Figs. 11 and 12) case, we predicted that the bandgap is calculated as 3 eV. Mehraz et al. performed experiments and concluded that with a 1% Sn doping, the bandgap is reduced 0.2 eV, which is similar to the reduction we predicted. When hydrogen is in the interstitial position, the bandgap reaches a value of 2.75 eV and mid-gap states are created at 1.95 eV. However, when H is substitutional of O, the bandgap reaches a value of 2.88 eV with gap states at 1.80 eV. From the above, it is expected that when TiO₂ is doped with carbon family elements, the bandgap is reduced with the most prominent reduction occurring with the Si Ti case. When hydrogen is inserted as a substitutional defect, the lowest bandgap is 2.70 eV for H0:SnTi:TiO₂. This value is one of the lowest bandgap values predicted for the doped TiO₂. For example, in the case of the halogen doped TiO₂, we had predicted in a
FIG. 8. Projected densities of states for (a) Si$_{Ti}$, (b) H$_8$ and Si$_{Ti}$, and (c) H$_{10}$ and Si$_{Ti}$ doped TiO$_2$.

FIG. 9. Densities of states for (a) Ge$_{Ti}$, (b) H$_8$ and Ge$_{Ti}$, and (c) H$_{10}$ and Ge$_{Ti}$ doped TiO$_2$. 
FIG. 10. Projected densities of states for (a) GeTi, (b) H\textsubscript{i} and GeTi, and (c) H\textsubscript{O} and GeTi doped TiO\textsubscript{2}.

FIG. 11. Densities of states for (a) SnTi, (b) H\textsubscript{i} and SnTi, and (c) H\textsubscript{O} and SnTi doped TiO\textsubscript{2}.
previous work that the lowest bandgap value (2.9 eV) is achieved with Cl:TiO$_2$. A significant reduction of the bandgap (2.43 eV) was achieved with Cr:TiO$_2$; however, it was under a constant pressure environment.

IV. CONCLUSIONS

In the present study, we performed calculations on the structural and electronic properties of TiO$_2$ in the cases of doping with X (C, Si, Ge, Sn) and co-doping with X and H. It is revealed that Si doping can significantly reduce the lattice parameters and the volume of the supercell. It is seen that in all the cases, hydrogen incorporation in interstitial and substitutional sites does not significantly alter the lattice parameters. To reveal the advantages of hydrogen co-doping on the Si-doped TiO$_2$, we performed DOS calculations and predicted that the most prominent bandgap reduction occurs when hydrogen sites to the oxygen position. Taking into account that in experiments there are many oxygen vacancies, it is expected that hydrogenation has a positive impact on the structural and electronic properties of TiO$_2$, thus making it a promising candidate for energy harvesting devices. We conclude that it is imperative to experimentally examine H:Si:TiO$_2$, as the bandgap reduction could be beneficial for energy device applications.

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The authors declare that there is no competing financial interest.

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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