Article

Measuring the Wall Thickness of a Trailing Arm Using Ultrasonic Measurement Model

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Abstract: Trailing arms are widely used in the automobiles’ suspension system, and effective detection of their wall thickness is essential to ensure their mechanical properties and to evaluate the casting process. In this work, an ultrasonic measurement model (UMM) is firstly established with consideration of the curvature and thickness of the trailing arm, then the UMM is introduced to predict the theoretical ultrasonic waveforms with different hypothetical thicknesses of the trailing arm. Next, the experimental ultrasonic waveforms are collected and matched with the predicted theoretical waveforms by using the correlation matching algorithm. The hypothetical thickness with the best match is regarded as the wall thickness of the trailing arm. Finally, an automatic ultrasonic experiment was conducted on a trailing arm with a 5-degrees of freedom (DOF) manipulator, in which the ultrasonic beam can radiate into a trailing arm at normal incidence. The results are compared with those determined by the micrometer and microscope, showing that their relative errors are controlled within 0.08 mm, which reveals the effectiveness of the present method. The method can also work for wall thickness measurements of curved components with CAD models.

Keywords: trailing arm; wall thickness; ultrasonic measurement model; Gaussian beam; curved surfaces

1. Introduction

The trailing arm is an important casting in the suspension system that connects the vehicle’s axle to its chassis; the wall thickness has a great impact on its quality in practical application [1,2]. The thickness tolerance can show the casting performance in manufacturing. Therefore, it is essential to accurately measure the thickness distribution of trailing arms.

Several methods can be adopted in thickness measurement [3], such as micrometer, eddy current, ultrasonic pulse-echo method [4], ultrasonic resonance method [5], etc. The micrometer measurement accuracy is high, but it cannot measure the wall thickness before destroying a trailing arm. Eddy current thickness gauge is mainly used for the thickness determination of the nonmagnetic coating upon the ferromagnetic material [3]. At present, commercial thickness gauges with the ultrasonic pulse-echo method have been widely used for thickness measurement [5,6]. Where a component with a curved surface is concerned, the thickness measurement accuracy is poor because the ultrasonic transducer cannot be coupled well with the component surface. The measurement accuracy is also affected by operators, while non-contact ultrasonic methods can overcome this limit because water can
act as couplant between the transducer and component [4], and the non-contact ultrasonic method can determine the thickness automatically with the ultrasonic measurement system. Where the ultrasonic resonance method is concerned, the calculation of theoretical resonance frequencies of double-curved components is complicated and sensitive to the inputs, and the matching errors of resonance frequencies are unavoidable in experiments.

It is well known that the accurate result of ultrasonic thickness measurement depends on both velocity and time of flight (TOF) [7]. However, the wall of a trailing arm has a double-curved surface, and the varying curvature can heavily distort the echoes of ultrasound, meaning that how to compensate and determine TOF is key to the problem. Although many papers regarding ultrasonic thickness measurement have been published, they cannot be directly applied to wall thickness measurement for double-curved components because they have not considered the curvatures.

In this work, an ultrasonic measurement model is introduced to predict theoretical waveforms for trailing arms in Section 2, and a correlation matching algorithm is developed to obtain the wall thickness by matching theoretical waveforms with the experimental waveform. Experiments with the 5-DOF ultrasonic testing system are presented in Section 3; the analysis is also included to show the validity of the present method. Finally, the conclusions are drawn in Section 4.

2. Method

2.1. The Overall Scheme

The overall scheme of the method is shown in Figure 1. The curvature, velocity, density and hypothetical wall thickness of the trailing arm are included to develop the ultrasonic measurement model; the theoretical ultrasonic waveform can be predicted for the trailing arm; ultrasonic experiment is conducted to obtain a real waveform, and then it is matched with the predicted waveform by using a correlation coefficient, which will be shown in Section 2.3. The hypothetical thickness is output as the measurement result if the correlation coefficient is a maximum.

Output the measurement result

Set correlation coefficient as $\rho_{x,y} = 0$; suppose hypothetical thickness $h_i (i = 1 \cdots N)$; $i = 1$

$h_i$, curvature, velocity, density, etc. are introduced to develop the ultrasonic measurement model

Conduct ultrasonic experiment

Obtain experimental waveform $y(t)$

Simulate the predicted waveform $y(t)$

Matching test; get $\rho'_{x,y}$

Thickness measurement result $h = h_i$

Figure 1. The overall flow chart of the thickness measurement.
2.2. An Ultrasonic Measurement Model for Trailing Arm

Figure 2 shows a pulse-echo ultrasonic measurement system with a focused transducer interrogating a trailing arm immersed in water. The sound beam emitted from the transducer T is incident on the outer surface S of the trailing arm along the normal direction of the interface. Some energy is reflected; the rest passes through the interface and propagates into the inner surface S. Reflection, refraction, and mode conversion will also occur at the S. Finally, part of the sound beam returns to the transducer T along the original path. The sound beam direction follows Snell’s law. The sound field is modeled to study the influence of the curvature and thickness on the waveform. In this work, the ABCD matrix and Multi-Gaussian beam [8] superposition method are used to establish the spatial sound field distribution model from transducer to trailing arm. The sound field distribution of frontwall and backwall can be written as [8–10]

\[
P_F(y, \omega) = \sum_{n=1}^{15} A^n \rho_f c_f v_0 \frac{\sqrt{\det M^n_1(d_1)}}{\sqrt{\det M^n_2(0)}} R_{12} \frac{\sqrt{\det M^n_1(d_1)}}{\sqrt{\det M^n_2(0)}} \cdot \exp \left( \frac{i \omega}{c_f} \left( \frac{d_1}{c_f} + \frac{d_2}{c_L} + \frac{1}{2} \frac{Y^T M^n_1(d_1) Y}{T_12} \right) \right)
\]

and

\[
P_B(y, \omega) = \sum_{n=1}^{15} A^n \rho_f c_f v_0 \frac{\sqrt{\det M^n_1(d_1)}}{\sqrt{\det M^n_2(0)}} R_{21} \frac{\sqrt{\det M^n_1(d_1)}}{\sqrt{\det M^n_2(0)}} \cdot \exp \left( \frac{i \omega}{c_f} \left( \frac{d_1}{c_f} + \frac{d_2}{c_L} + \frac{d_1}{c_f} + \frac{1}{2} \frac{Y^T M^n_1(d_1) Y}{T_21} \right) \right)
\]

where \( Y = [y_1 y_2], y = [y_1 y_2 y_3], A \) is Gaussian coefficient, \( n \) is the serial number of the Gaussian coefficient, \( \omega \) is the beam frequency, \( y \) is the spatial distribution of the sound field at the receiver, \( Y \) is a section perpendicular to the direction of sound beam propagation \( y_3, v_0 \) is the surface velocity of the transducer, \( \rho_f \) is the density of water, \( c_f \) is the velocity of sound in water, \( c_L \) is the velocity of sound in solid, \( d \) is the unit vector of sound beam propagation direction, \( d_1 \) is water path, \( d_2 \) is the sound beam propagation distance in the trailing arm, which is the wall thickness \( h \) of the target incident point. \( T_{12} \) and \( T_{21} \) are transmission coefficients, which are related to curvature \( \kappa_1, \kappa_2, \kappa_3 \) and \( \kappa_4 \). \( R_{21} \) is the reflection coefficient. \( M^n_1 \) and \( M^n_2 \) are the \( 2 \times 2 \) matrix related to the amplitude and phase of the sound beam in sound beam propagation.

The derivation and calculation of the above parameters can be found in Reference [11]. In a linear ultrasonic testing system, the strength of the received signal depends on the strength of the sound field received by the transducer, and the sound field received by the transducer is the response of each particle on the surface of the transducer. The average sound pressure on the surface of the transducer is used to indicate the strength of the received sound field, also known as transfer function, expressed as [9,12]:

\[
\bar{P}(\omega) = \frac{\int_S P(y, \omega) dS}{S}
\]

Ultrasonic measurement model includes two main parts: one is the system function, \( s(\omega) \), which only considers all the electrical and electromechanical parts in the measurement system; and the other is the elastic/acoustic transfer function, \( \bar{P}(\omega) \), which describes the propagation, reflection, scattering, and reception processes of ultrasonic acoustics. The ultrasonic measurement model can be written as [9,12]

\[
V_R(\omega) = s(\omega) \bar{P}(\omega)
\]

In practical applications, the system influence factor is usually obtained by a direct measurement in a calibration setup, where the pulse-echo wave from a front planar surface at normal incidence is
measured [13]. Combing the system function and transfer function, the frontwall and backwall echo can be predicted according to Equation (4).

Thus, the approximate error of these two waveforms is obtained.

\[ x_e(t) = x(t) - a_{xy} y(t + \tau) \]  

(6)

According to the minimum mean square error criterion, we know that:

\[ \overline{x_e^2(t)} = \int_{-\infty}^{\infty} [x(t) - a_{xy} y(t + \tau)]^2 dt \]  

(7)

when \( \overline{x_e^2(t)} \) is minimum, these two waveforms match best, and we can get.

\[ a_{xy} = \frac{\int_{-\infty}^{\infty} \overline{x(t) y(t + \tau)} dt}{\int_{-\infty}^{\infty} \overline{y^2(t)} dt} \]  

(8)

Substituting Equation (8) into Equation (7), the minimum approximation error can be obtained as:

\[ \overline{x_e^2(t)} = \int_{-\infty}^{\infty} \overline{x^2(t)} dt - \left[ \frac{\int_{-\infty}^{\infty} \overline{x(t) y(t + \tau)} dt}{\int_{-\infty}^{\infty} \overline{y^2(t)} dt} \right]^2 \]  

(9)

Use waveform \( x(t) \) to normalize the minimum error,

\[ \bar{e}_{\text{min}} = \frac{\overline{x_e^2(t)}_{\text{min}}}{\int_{-\infty}^{\infty} \overline{x^2(t)} dt} = 1 - \left[ \frac{\int_{-\infty}^{\infty} \overline{x(t) y(t + \tau)} dt}{\int_{-\infty}^{\infty} \overline{x^2(t)} dt \int_{-\infty}^{\infty} \overline{y^2(t)} dt} \right]^2 \]  

(10)
Define that [15],

\[
\rho_{xy} = \frac{\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \bar{x}(t) \bar{y}(t+\tau)dt^2}{\int_{-\infty}^{\infty} \bar{x}^2(t)dt \int_{-\infty}^{\infty} \bar{y}^2(t)dt}
\]  

(11)

\(\rho_{xy}\) is the correlation coefficient of waveforms \(x(t)\) and \(y(t)\), and the integral is converted into a numerical operation to obtain [15].

\[
\rho_{xy} = \frac{(\sum x(t)y(t+\tau))^2}{\sum (x(t))^2 \sum (y(t+\tau))^2}
\]  

(12)

\(\rho_{xy} = 1\) means two waveforms are completely correlated, \(\rho_{xy} = 0\) means the two signals are completely uncorrelated and \(0 < \rho_{xy} < 1\) means partially correlated. These two waveforms match better when \(\rho_{xy}\) is bigger [16].

Where the hypothetical wall thickness is concerned, the time of flight of the experimental waveform \(y(t)\) is used to calculate the approximate thickness, and a gap of 0.01 mm is introduced to create the hypothetical wall thicknesses based on the approximate thickness with ±30% range.

3. Experiments and Analysis

3.1. Ultrasonic Measurement Analysis

Figure 3a depicts the setup for ultrasonic experiments [17]. A DPR 300 ultrasonic pulse generator/receiver was employed to drive a spherically focused transducer (Panametrics V327, 2-inch focal length, Olympus Panametrics, Inc., Waltham, MA, USA) with the center frequency of \(f_0 = 9.78\) MHz, the effective element radius of \(r = 6.35\) mm and the pulse width of \(\sigma = 0.52\) μs. Then, a computer-controlled 5-DOF manipulator was used to hold and adjust the transducer so that the ultrasonic beam can radiate into the trailing arm in the water tank at normal incidence [18]. Finally, a 200 MHz DAQ data acquisition card ADLINK PCIe-9852 was adopted to obtain the ultrasonic waveforms. The density and longitudinal velocity of the trailing arm were measured as \(\rho = 7836\) kg/m³, \(c_L = 5750\) m/s. The density and longitudinal velocity of water were measured as \(\rho_f = 1000\) kg/m³, \(c_L = 1486\) m/s. Curvature parameters are determined by the CAD model of the trailing arm.

![Automatic ultrasonic measurement setup](image)

Figure 3. Automatic ultrasonic measurement: (a) experimental setup; (b) a trailing arm.

As shown in Figure 3b, twelve points are selected from the trailing arm for thickness measurement, and three experimental waveforms are collected at each point. Since ultrasonic has a strong directivity, the incident direction of the acoustic beam shall be in agreement with the direction of normal vector of the point when ultrasonic signals are acquired [18], thus, the kinematic equation [19] for the 5-DOF manipulator is established according to the Denavit–Hartenberg parameters [20] and the CAD model of the manipulator. All the joint variables can be inversely resolved from the kinematic equation of the manipulator [20]. The acoustic beam is then aligned with the points on the trailing arm by adjusting the attitude of the transducer. Please refer to the published work for details [18].
3.2. Measurement Results Analysis

According to the above-mentioned method, the ultrasonic waveforms obtained in the experiments are used to match with predicted waveforms, and three measurement results are averaged for the wall thickness of a certain point to suppress the random error, Table 1 shows the measurement results for a trailing arm.

| Measurement No. | Point No. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|----------------|-----------|---|---|---|---|---|---|---|---|---|----|----|----|
| 1              |           | 4.15 | 5.18 | 4.98 | 6.22 | 5.73 | 4.83 | 5.14 | 5.45 | 6.32 | 5.70 | 5.01 | 5.22 |
| 2              |           | 4.17 | 5.23 | 5.03 | 6.28 | 5.74 | 4.82 | 5.10 | 5.49 | 6.28 | 5.66 | 4.97 | 5.26 |
| 3              |           | 4.16 | 5.22 | 5.02 | 6.25 | 5.69 | 4.84 | 5.15 | 5.44 | 6.33 | 5.65 | 4.99 | 5.27 |
| mean           |           | 4.16 | 5.21 | 5.01 | 6.25 | 5.72 | 4.83 | 5.13 | 5.46 | 6.31 | 5.67 | 4.99 | 5.25 |

To further illustrate the matching process of the proposed method, Figure 4 indicates an experimental waveform and two predicted waveforms when $h$ are 5.74 and 5.85 mm, and their correlation coefficients are 0.92 and 0.81, respectively. One can see from Figure 4 that the predicted waveform matches with experimental waveform better when the correlation coefficient is bigger. Note that these two predicted waveforms are calculated using the same parameters with different angles of incidence ($2^\circ$ and $0^\circ$), which shows that it is necessary for the ultrasonic beam to radiate into the trailing arm at normal incidence.

To verify the validity of automatic ultrasonic measurement, the trailing arm undergoes subdivision, stripping, and slicing, then the thickness measurement is performed on the planned points with a micrometer (Mitutoyo, M110-25), whose specification of measurement error is 0.01 mm. Table 2 shows the results measured with different methods and their relative errors. As this shows, the relative errors between the results measured with micrometer and the present method are within 0.08 mm, which meets the measurement requirement of a trailing arm manufactured by casting. Because the relative errors between the results measured with micrometer and the conventional ultrasonic thickness measurement method are much higher, the ultrasonic measurement accuracy will degrade if the curvature is not taken into consideration. In addition, Measurement with an Olympus SZX16 stereomicroscope is performed; Figure 5 indicates its measurement result of point 3, which agrees well the result determined by the present method.

![Waveform matches at different correlation coefficients.](image-url)
Table 2. Comparisons between results measured with three different methods.

| No. | Results Measured with Micrometer (mm) | Results of Present Method (mm) | Relative ErrorI (mm) | Results of Conventional Ultrasonic Method (mm) | Relative ErrorII (mm) |
|-----|-------------------------------------|-------------------------------|---------------------|-----------------------------------------------|----------------------|
| 1   | 4.20                                | 4.16                          | 0.04                | 3.98                                          | 0.22                 |
| 2   | 5.15                                | 5.21                          | 0.06                | 5.03                                          | 0.12                 |
| 3   | 5.06                                | 5.01                          | 0.05                | 4.93                                          | 0.13                 |
| 4   | 6.17                                | 6.25                          | 0.08                | 6.34                                          | 0.17                 |
| 5   | 5.79                                | 5.72                          | 0.07                | 5.47                                          | 0.32                 |
| 6   | 4.76                                | 4.83                          | 0.07                | 4.92                                          | 0.25                 |
| 7   | 5.18                                | 5.13                          | 0.05                | 5.09                                          | 0.09                 |
| 8   | 5.53                                | 5.46                          | 0.07                | 5.39                                          | 0.14                 |
| 9   | 6.23                                | 6.31                          | 0.08                | 6.34                                          | 0.11                 |
| 10  | 5.75                                | 5.67                          | 0.08                | 5.88                                          | 0.13                 |
| 11  | 4.93                                | 4.99                          | 0.06                | 5.01                                          | 0.08                 |
| 12  | 5.33                                | 5.25                          | 0.08                | 5.21                                          | 0.12                 |

P.S.: Relative Error I denotes relative error between the present ultrasonic method and micrometer method. Relative Error II denotes relative error between the conventional ultrasonic method and micrometer method.

Figure 4. Waveform matches at different correlation coefficients.

To verify the validity of automatic ultrasonic measurement, the trailing arm undergoes subdivision, stripping, and slicing, then the thickness measurement is performed on the planned points with a micrometer (Mitutoyo, M110-25), whose specification of measurement error is 0.01 mm. Table 2 shows the results measured with different methods and their relative errors. As this shows, the relative errors between the results measured with micrometer and the present method are within 0.08 mm, which meets the measurement requirement of a trailing arm manufactured by casting. Because the relative errors between the results measured with the micrometer and the conventional ultrasonic thickness measurement method are much higher, the ultrasonic measurement accuracy will degrade if the curvature is not taken into consideration. In addition, measurement with an Olympus SZX16 stereomicroscope is performed; Figure 5 indicates its measurement result of point 3, which agrees well with the result determined by the present method.

Figure 5. Workpiece thickness measured by experiment.

The limitations for the applicability of the used approach include: CAD model of the component to be measured is required, the transducer must be carefully controlled so that ultrasonic beam radiates into the trailing arm at normal incidence, otherwise the experimental waveform cannot be obtained accurately, which results in measurement error. The measurement efficiency of the present method is not high; it generally takes 25 min to finish a trailing arm measurement.

4. Conclusions

In this work, an automatic measurement method was developed to measure the wall thickness of trailing arms nondestructively; the method can also work for wall thickness measurement of curved components with CAD models. The conclusions are drawn as follows:

- Both the curvature and thickness of the trailing arm are both introduced to calculate the predicted waveforms, so the present method has obvious advantages over the conventional ultrasonic thickness measurement method;
A waveform matching method is developed to calculate the measured thickness;

The relative errors between the results determined by the present method and micrometer are within 0.08 mm, but the present method does not need to destroy the trailing arm.

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**References**

1. Kang, O.; Park, Y.; Park, Y.S.; Suh, M. Look-ahead preview control application to the high-mobility tracked vehicle model with trailing arms. *J. Mech. Sci. Technol.* **2009**, *23*, 914–917. [CrossRef]

2. Margolis, D. The stability of trailing arm suspensions in heavy trucks. *Int. J. Veh. Des.* **2001**, *25*, 211–229. [CrossRef]

3. Lian, M.; Liu, H.; Zhang, T.; Bo, Q.; Li, T.; Wang, Y. Ultrasonic on-machine scanning for thickness measurement of thin-walled parts: Modeling and experiments. *Int. J. Adv. Manuf. Technol.* **2019**, *104*, 2061–2072. [CrossRef]

4. Han, Z.R.; Fan, Z.J.; Xiao, Y.; Jia, Z. A research on thickness distribution of oblique cone in dieless shear spinning. *Int. J. Adv. Manuf. Technol.* **2017**, *90*, 2901–2912. [CrossRef]

5. Huang, N.; Yin, C.; Lian, M.; Hu, J.; Wu, S. Error compensation for machining of large thin-walled part with sculptured surface based on on-machine measurement. *Int. J. Adv. Manuf. Technol.* **2018**, *96*, 4345–4352. [CrossRef]

6. Cong, S.; Gang, T. Ultrasonic thickness measurement for aluminum alloy irregular surface parts based on spectral analysis. *Trans. Nonferr. Met. Soc. China* **2012**, *22*, S323–S328. [CrossRef]

7. Zhou, L.J.; Liu, H.B.; Lian, M.; Ying, Y.W.; Li, T.; Wang, Y.Q. Highly accurate adaptive TOF determination method for ultrasonic thickness measurement. *Meas. Sci. Technol.* **2018**, *29*, 045002. [CrossRef]

8. Schmerr Jr, L.W.; Sedov, A. Multi-Gaussian ultrasonic beam modeling for multiple curved interfaces-An ABCD matrix approach. *Res. Nondestruct. Eval.* **2005**, *16*, 143–174. [CrossRef]

9. Zhang, S.; Hu, P.; Li, X.; Jeong, H. Calibration of focused circular transducers using a multi-Gaussian beam model. *Appl. Acoust.* **2018**, *133*, 182–185. [CrossRef]

10. Schmerr Jr, L.W.; Song, S-J. *Ultrasonic Nondestructive Evaluation Systems*; Springer: New York, NY, USA, 2007; pp. 154–196.

11. Kim, H.J.; Schmerr, L.W.; Sedov, A. Generation of the basis sets for multi-Gaussian ultrasonic beam models. In *Review of Progress in Quantitative Nondestructive Evaluation, Proceedings of the 31st Annual Review of Progress in Quantitative Nondestructive Evaluation, Colorado Sch Mines, Golden, CO, USA, 25–30 July 2004*; Thompson, D.O., Chimenti, D.E., Eds.; American Institute of Physics: New York, NY, USA, 2005. [CrossRef]

12. Zhang, S.; Li, X.; Jeong, H. Analytical Diffraction Corrections for Circular Focused Transducers Expressed Using the Multi-Gaussian Beam Model. *Acta Acust. United Acust.* **2017**, *103*, 717–720. [CrossRef]

13. Wang, W.; Liu, X.; Li, X.; Xu, G.; Zhang, S. Modeling Flaw Pulse-Echo Signals in Cylindrical Components Using an Ultrasonic Line-Focused Transducer with Consideration of Wave Mode Conversion. *Sensors* **2019**, *19*, 2744. [CrossRef] [PubMed]

14. MacCoss, M.J.; Wu, C.C.; Liu, H.B.; Sadygov, R.; Yates, J.R. A correlation algorithm for the automated quantitative analysis of shotgun proteomics data. *Anal. Chem.* **2003**, *75*, 6912–6921. [CrossRef] [PubMed]

15. Tsui, P.H. Minimum Requirement of Artifical Noise Level for Using Noise-Assisted Correlation Algorithm to Suppress Artifacts in Ultrasonic Nakagami Images. *Ultrasound. Imaging* **2012**, *34*, 110–124. [CrossRef] [PubMed]

16. Taylor, R. Interpretation of the Correlation Coefficient: A Basic Review. *J. Diagn. Med Sonogr.* **1990**, *6*, 35–39. [CrossRef]
17. Li, X.B.; Zhou, X.J.; Zheng, H.F. Data compression for ultrasonic inspection. *J. Zhejiang Univ. (Eng. Sci.)* 2008, 42, 1251–1254. [CrossRef]

18. Li, X.; Hu, H.; Yang, Y.; Ni, P.; Yang, C. Automatic ultrasonic inspection of flaws in a propeller-blade. *Nondestruct. Test. Eval.* 2010, 25, 341–351. [CrossRef]

19. Balkan, T.; Ozgoren, M.K.; Arikan, M.A.S.; Baykurt, H.M. A kinematic structure-based classification and compact kinematic equations for six-dof industrial robotic manipulators. *Mech. Mach. Theory* 2001, 36, 817–832. [CrossRef]

20. Lee, B.J. Differential Kinematics of Flexible Manipulator for Calibration of Model Parameters. *Adv. Intell. Syst. Comput.* 2013, 208, 359–373. [CrossRef]

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