Thermal comfort in the low energy building - validation and modification of the Fanger model

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Abstract. Nowadays, we spend most of our time inside buildings. Thus, ensuring adequate thermal comfort is an important issue. The paper discusses the issue of thermal comfort assessment in the intelligent low energy building “Energis” of Kielce University of Technology (Poland). The tests conducted in a selected lecture theater focused on collecting anonymous questionnaires containing thermal sensation and air quality votes of the respondents as well as performing measurements of indoor air parameters (air and globe temperatures, relative humidity, air velocity and CO₂ concentration). Based on the obtained data a comparison has been done between the actual sensation votes of the volunteers and the calculation results performed with the Fanger thermal comfort model. Two indices have been considered in the paper: PMV (Predicted Mean Vote) and PPD (Predicted Percentage Dissatisfied). A modification of the model has also been proposed, which considers the impact of the carbon dioxide concentration on thermal comfort.

1 Introduction

The issue of thermal comfort is of increasing importance in the existing world. Nowadays, an increasing number of people spend their time indoors. This increases the interest in the conditions in a given room. More and more people are trying to ensure thermal comfort by using appropriate air-conditioning and heating devices. Proper thermal conditions are key elements for our well-being, health and productivity. Not providing the right conditions can adversely affect our immune system and we start to feel tired. Our efficiency of performed activities will also decrease, which will make us less efficient regardless of whether the work is mental or physical. That is why it is so important to ensure adequate parameters of the air in the room and try to keep them at an appropriate, as far as possible unchanging level. Despite many years of research on this topic, many questions still remain unanswered.

Thermal comfort is the state of human satisfaction with the conditions of the room in which they stay. Our body does not feel cold or too warm then. In general, a person's feeling of thermal comfort has a significant impact on the efficiency of their work. Failure to ensure appropriate air parameters may lead to a reduction in the effectiveness of the activities performed. The main parameters influencing the determination of thermal comfort are air temperature and velocity, relative humidity, average radiation temperature and physical activity. Air temperature is the main factor affecting thermal comfort. It’s too high or too low value causes that a person does not feel comfortable in a given room. The human body can function in a very wide temperature range, but only to a small extent it feels thermal comfort. The most popular method to determine thermal comfort is the Fanger model [1]. This model was developed in the 1970s by O. Fanger and is the basis of the applicable standards: ISO 7730 [2] together with PN-EN 16798-1: 2019 [3]. The Fanger model is related to the following two indicators: PMV, defined as the Predicted Mean Vote, and PPD, which is the Predicted Percentage of Dissatisfied people. The PMV index is expressed using a seven-point scale according to the American standard ASHRAE 55 [4], which is on a scale from -3 to +3, where negative means cold and positive means hot. According to the Fanger model, for the thermal environment to be acceptable for most buildings, the PMV value must be between -0.5 and 0.5 for most buildings. It is assumed that humans prefer a neutral thermal environment, i.e., a PMV value of zero, as a comfortable thermal environment.

The Fanger model practically comes down to the following equation according to [2]:

\[
\text{PMV} = \left[ 0.303 \cdot \exp(-0.036 \cdot M) + 0.028 \right] \cdot \\
\left[ (M - W) - 3.05 \cdot 10^{-3} \cdot (5733 - 6.99 \cdot (M - W) - p_a) - 0.42 \cdot ((M - W) - 58.15) - 1.7 \cdot 10^{-5} \cdot M \cdot (5867 - p_a) - 0.0014 \cdot M \cdot (34 - t_a) - 3.96 \cdot 10^{-8} \cdot f_{cl} \cdot \left( (t_{cl} + 273)^4 - (t_c + 273)^4 \right) - f_{cl} \cdot h_c \cdot (t_{cl} - t_a) \right] \tag{1}
\]

where: M - metabolic rate [W/m²], W - effective mechanical power [W/m²], Lᵢ - thermal insulation of clothing [m²K/W], tᵦ - air temperature [°C], tᵣ - average
radiation temperature [°C], \( p_a \) - partial pressure of water vapour [Pa], \( t_{cl} \) - surface temperature of clothing [°C].

Over the past few years, many scientists have studied the difference between thermal sensations and PMV. Aghniaey et al. [5,6] conducted research on thermal comfort on a university campus in the United States. The study measured the following parameters: temperature and air velocity, relative humidity, \( \text{CO}_2 \) concentration, and average radiation temperature. The results showed that the respondents preferred higher temperature ranges, especially women accept a warmer environment. Majewski et al. [7] conducted research in an intelligent building and noticed differences between the actual and forecast values of thermal comfort. Broday et al. [8] analysed thermal comfort by comparing Fanger's model with people's real thermal sensations. The authors [9] used a thirteen-degree scale of thermal comfort for the thermal comfort tests instead of the seven-level scale used according to ISO 7730 [2]. They found that the thermal sensations of the respondents were satisfactory in the range of -0.5 to +0.5. Almeida et al. [10] conducted studies in school buildings where they examined the relationship between PMV and Mean Thermal Sensation (MTS) and operating temperature. They concluded that there was a significant relationship between them. The article [11] presents the Fanger model for air-conditioned office buildings and presents the differences between the model and survey results. Djamila [12] analysed the influence of individual microclimate elements on thermal comfort. Jazizadeh et al. [13] conducted research in office buildings in terms of thermal comfort. They concluded that the most important factor influencing thermal comfort is air temperature. Mors et al. [14] conducted research in school buildings and observed a significant difference between the PMV determined by the standard and the survey data. Luo et al. [15] determined that thermal comfort was significantly influenced by an increase in the metabolic rate. The research presented by Vilcekova et al. [16] showed a discrepancy between the results of PMV calculations and the actual sensations. The results also showed an increase in \( \text{CO}_2 \) concentration during school classes. Enescu [17] presents models and indicators for thermal sensation and shows that validation of thermoregulation models is difficult, which contributes to increased interest. The latest research is improving the models. In Poland, studies on thermal comfort and indoor air quality were conducted, among others, by Dudkiewicz et al. [18], Majewski et al. [7], Piotrowski et al. [19].

The article analyses the thermal comfort in an intelligent building together with the feelings of the people examined. Two indicators PMV and PPD were taken into account and a modification of the PMV equation was proposed based on preliminary test results. The motivation behind the paper is the fact that many studies found in literature report that there are differences between the actual thermal sensations of people and the Fanger model and still this issue is not solved.

### 2 Material and method

The research was conducted in the autumn of 2020 in the intelligent building "Energis" of the Kielce University of Technology. Figure 1 below presents a photo of the building from the Western side.

![Figure 1. Photo of the "Energis" building.](image)

The study was conducted in a lecture hall on the first floor with mechanical ventilation (marked in red in the figure). The intelligent Energis building has been designed to provide adequate air parameters for its occupants. Air-conditioning and heating devices significantly affect the conditions in the room, therefore the designed air-conditioning and heating systems should ensure appropriate parameters, depending on the purpose of the room. The next figure shows the room where tests were done (with thermal images generated by an infrared camera - Fig. 2).

![Figure 2. Lecture room no 1.14: a) photos, b) thermal images.](image)
parameters in the rooms. A microclimate meter was used to determine the air parameters. The probes were placed at the height of the respondents, at the level of the thermal centre of gravity. Parameters such as temperature and air velocity, relative humidity, carbon dioxide concentration and light intensity were measured. The measurement accuracy of the measured parameters are as follows: for the indoor air temperature it is +/- 0.3 °C, air flow velocity: +/- 0.03 m/s, relative humidity: +/- 2 % and concentration of CO₂: +/- 50 ppm. Local comfort issues such as Draught Rate or Turbulence Intensity were not taken into account in the surveys conducted due to their marginal impact in this kind of building (the velocity was quite uniform in the area where the students were). The graph below shows how carbon dioxide changes over time. It was considered sufficient due to the fact that the value stabilised (changes did not exceed the accuracy of CO₂ detection).

![Figure 3](image)

**Figure 3.** Graph of carbon dioxide changes over time.

From the graph, it can be concluded that carbon dioxide increases with time. During the increase in carbon dioxide, students sit in the test room. The greatest increase can be seen after about 160 seconds. After this time, the curve continues to rise, but not so sharply. The concentration of carbon dioxide in a room depends on the number of people staying in it. The more people in the room, the faster the carbon dioxide amount curve will rise. In the tested room, the concentration of carbon dioxide did not exceed the permissible concentration of about 5000 ppm [20] (the threshold of 5000 ppm is actually quite high comparing to the values in air quality standards), because the classroom has a large area. With higher carbon dioxide, a person feels discomfort. During the stabilization of the air parameters, the participants completed questionnaires concerning the feeling of thermal sensations in the room. Below is a picture of the microclimate meter that was used to measure air parameters and the students completing the questionnaires (Figure 4).

![Figure 4](image)

**Figure 4.** Photograph of the measuring device Testo 400 with probes.

### 3 Results and discussion

The research was conducted in the fall with 54 participants, 15 women and 39 men aged 18 to 21 years. The experimental programme involved questions on thermal sensations, acceptability, preferences and others, however on Figure 5 only the frequency of answers about the thermal sensations votes (TSV) in the rooms studied has been given. This parameter defines how individual people assess their thermal environment.

![Figure 5](image)

**Figure 5.** The frequency of the answers on thermal sensations votes: “-3” - too cold, “-2” - too cool, “-1” - pleasantly cool, “0” - comfortable, “1” - pleasantly warm, “2” - too warm, “3” - too hot.

The conducted research shows that the “too cold” option was 3.7%, i.e., 2 people out of 54 people chose this answer. The answer “too warm” was repeated as much as “too cold”. The respondents answered “too cool” 5 times, which is 9.26%. The answer “pleasantly cool” was selected 8 times, i.e., the frequency was 14.81%. The most frequently given answer was the “comfortable” option. It constitutes 51.85% of all questionnaires completed by the respondents. In the case of the “pleasantly warm” answer, its frequency was 16.67%. There is also a Gaussian curve in the graph that represents the distribution of the normal. Comparing the results of the conducted research, it can be concluded that the students did not feel well in the room under
study. This means that there was no thermal comfort because the percentage of selecting “too cold”, “too warm”, “too warm” and “too hot” was greater than 10%. It amounted to 16.67%, which is how many people were dissatisfied with the prevailing conditions. Figure 6 shows the frequency of answers about the air quality in the rooms studied has been given.

Figure 6. The frequency of answers given by the respondents regarding air quality: “-2” - very bad, “-1” - bad, “0” - neither good nor bad, “1” - good, “2” - very good.

The conducted research on air quality assessment shows that the most common answer given by the respondents was the answer “good” and it amounted to 62.96%, which corresponds to 34 responses out of 54. The second largest number of answers selected is the option “neither good nor bad”. It repeated 19 times, i.e., its frequency is 35.19%. The “bad” option is 1.85%.

During the research, at the end of the questionnaire, the respondents completed a with information on the subject's sex, age, height and weight. This was used to calculate the BMI (body mass index) and compared it to thermal voices of the volunteers (Figure 7). Body mass index is a ratio of mass (in ‘kg’) over height (in ‘m’) to the second order.

Figure 7. Dependence of TSV on the BMI mass index.

Based on the results, it can be concluded that people with BMI in the range of less than 20 rate their thermal sensation vote as cold, while with an index between 22 and 26 they feel comfortable. The study shows that the higher the BMI range, the higher the thermal sensation vote. Consequently, people with higher BMI tend to prefer lower temperature, with lower BMI the opposite is true. Below in Figure 8 is a graph showing the respondents' thermal sensations vote (TSV) and thermal preferences vote (TPV) – which describes the preferences of people on the temperature value in the room.

Figure 8. Thermal sensations vote (TSV) and thermal preferences vote (TPV) of the respondents.

The graph shows the thermal impressions and thermal preferences of the respondents. Average TSV and TPV scores were calculated for each room. From the above graph, it can be seen that those who felt comfortable (TSV = 0) would like the room to be no changed (TPV = 0). When comparing the distribution of scores based on thermal sensation vote (TSV) and thermal preference vote (TPV), it can be observed that most of the subjects preferred the conditions they were in. Overall, during the study, students rated their thermal environment as warm, while their thermal preferences varied. During the tests, the concentration of carbon dioxide was also determined. Figure 9 shows the air temperature and the concentration of carbon dioxide in the lecture room as well as other rooms tested earlier by the author and considered for the model modification (similar number of people – students were present in those rooms).
Figure 9. Air temperature and CO₂ concentration in rooms.

The figure above shows the indoor temperature and carbon dioxide data. The research results were based on the results from the literature [21, 22] and the results from the autumn 2020 period. Carbon dioxide has a significant impact on air quality; therefore, this phenomenon requires further research. However, it needs to be reported that the data indicate a relatively low level of CO₂ in the studied educational rooms.

Based on the experimental data of questionnaires and direct measurements, the Fanger model was modified considering the impact on carbon dioxide, as shown in formula (2) below:

\[
PMV = \left[0.303 \cdot \exp(-0.036 \cdot M) + 0.028\right] \cdot (-0.00015) \cdot CO_2 \cdot [(M - W) - 3.05 \cdot 10^{-3} \cdot [5733 - 6.99 \cdot (M - W) - p_d] - 0.42 \cdot [(M - W) - 58.15] - 1.7 \cdot 10^{-5} \cdot M \cdot (5867 - p_a) - 0.0014 \cdot M \cdot (34 - t_w) - 3.96 \cdot 10^{-8} \cdot f_c \cdot [(t_{cl} + 273)^4 - (t_r + 273)^4] - f_c \cdot h_c \cdot (t_{cl} - t_a)\]
\]

(2)

Equation (2) was extended by the product (-0.00015) \cdot CO₂, which “brought” the results from the research closer to the trend line. The next figure shows the results of PMV and TSV and after model modification.

Figure 10. Modification of the Fanger model.

The above graph represents a modification of the Fanger model including the impact of carbon dioxide. Green points mark the results of measurements from previous tests [21, 22]. Black points are the current research (from surveys and calculations according to Fanger's formula), while blue points are the results after model modification. The red trend line indicates 100% compliance with the model. One may notice that the results marked in blue are closer to the trend line than the rest of the results. The chart shows a significant improvement when modifying the formula.

Another index is PPD. Its comparison from the questionnaires and model calculation results indicates significance differences, as shown below (Fig. 11).

Figure 11. Comparison of actual test results and calculations according to the Fanger model for PPD.

On the basis of the presented figure, it can be seen that the values of the predicted percentage of dissatisfied people do not coincide with the Fanger model. The standard [3] stipulates that the percentage of people dissatisfied with the microclimate should not exceed 10% for these types of buildings. It can be concluded that this value has not been met in an intelligent building Energis, where tests were conducted.

4 Conclusions

The research carried out in an intelligent building showed that the number of people dissatisfied with the prevailing conditions exceeded 10%. Most people prefer a warmer environment, so this could explain the number of dissatisfied people. When analysing the Fanger model, it can be seen that it differs from the responses of people participating in the study regarding thermal comfort. The current model provides a comfortable temperature, which is actually too high for the respondents. Modification of the model taking into account the influence of carbon dioxide concentration on thermal comfort resulted in the results of the surveys being consistent with the ideal model (TSV ≅ PMV).

When assessing the predicted number of dissatisfied people (PPD), it can also be noticed that the results of the respondents do not coincide with the Fanger's model. Further work should therefore be done on this topic to create an even more accurate model, especially that the number of test rooms was quite limited. The study is a preliminary study and currently, due to the pandemic situation, the number of research results is limited, but it will be expended.

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