Domain Adaptation for the Segmentation of Confidential Medical Images

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Abstract

Convolutional neural networks (CNNs) have led to significant improvements in the semantic segmentation of images. When source and target datasets come from different modalities, CNN performance suffers due to domain shift. In such cases data annotation in the target domain becomes necessary to maintain model performance. To circumvent the re-annotation process, unsupervised domain adaptation (UDA) is proposed to adapt a model to new modalities using solely unlabeled target data. Common UDA algorithms require access to source domain data during adaptation, which may not be feasible in medical imaging due to data sharing restrictions. In this work, we develop an algorithm for UDA where the source domain data is inaccessible during target adaptation. Our approach is based on encoding the source domain information into an internal distribution that is used to guide adaptation in the absence of source samples. We demonstrate the effectiveness of our algorithm by comparing it to state-of-the-art medical image semantic segmentation approaches on two medical image semantic segmentation datasets.

1 Introduction

Employing CNNs in semantic segmentation tasks has been proven to be extremely helpful in various applications, including object tracking [4, 67, 75], self-driving cars [20, 29], and medical image analysis [1, 27, 28, 55]. This success, however, is conditioned on the availability of huge manually annotated datasets to supervise the training of state-of-the-art (SOTA) network structures [50, 60]. This condition is not always realized in practice, especially in fields such as medical image segmentation, where annotating data requires the input of trained experts and privacy regulations make sharing data for crowd-sourcing extremely restricted, and at times impossible. A characteristic of data in the area of medical image segmentation is the existence of domain shift between different imaging modalities, which stems from using imaging devices based on totally different electromagnetic principles, e.g., CT vs MRI. When domain gap exists between the distributions of the training (source) and the testing (target) data, the performance of CNNs can degrade significantly. This makes continual data annotation necessary for maintaining model performance.
Domain shift is a major area of concern, as data annotation is a challenging procedure even for the simplest semantic segmentation tasks [38]. Annotating medical images is also expensive, as annotation can be performed only by physicians, who undergo years of training to obtain domain expertise. Unsupervised domain adaptation (UDA) is a learning setting aimed at reducing domain gap without data annotation in the target domain. The goal is to adapt a source-trained model for improved generalization in the target domain using solely unannotated data [18, 52, 64, 70]. The core idea in UDA is to achieve knowledge transfer from the source domain to the target domain by aligning the latent features of the two domains in an embedding space. This idea has been implemented either using adversarial learning [5, 16, 21, 63], directly minimizing the distance of distributions of the latent features with respect to a probability metric [7, 35, 48, 58], or a combination of the two [12, 54].

While existing UDA algorithms have been successful in reducing cross-domain gap, the vast majority of these approaches require sharing data between the source and target domains to enforce distribution alignment. This requirement limits the applicability of most existing works when sharing data may not be possible, e.g., sharing data is heavily regulated in healthcare domains due to the confidentiality of patient data and from security concerns. Until recently, there has been little exploration of UDA when access to the source domain is limited [30, 45, 49, 53, 66]. These recent works benefit from generative adversarial learning to maintain source distribution information. However, addressing UDA for classification tasks limits the applicability of such methods to the problem of organ semantic segmentation [73]. A similar problem is encountered with UDA for street semantic segmentation [31], given medical devices produce data distributions requiring additional preparation with large background areas [74]. Recent medical works propose adaptation without source access via entropy minimization [2, 3], but these methods are susceptible to degenerate solutions.

**Contribution:** we develop a UDA algorithm for the semantic segmentation of medical images when sharing data is infeasible due to confidentiality or security concerns. Our approach is able to reduce domain gap without having direct access to the source data during adaptation. We learn the internal distribution for the source domain, and transfer knowledge between the source and target domains by distribution alignment between the learned internal distribution and the latent distribution of features of the target domain. We validate our algorithm on two medical image segmentation datasets, and observe comparable performance to SOTA methods based on joint training.

## 2 Related Work

SOTA semantic segmentation algorithms use deep neural network architectures to exploit large annotated datasets [34, 36, 39, 43]. These approaches are based on training a CNN encoder using manually annotated segmentation maps to learn a latent embedding of the data. An up-sampling decoder combined with a classifier is then used to infer pixel-wise estimations for the true semantic labels. Performance of such methods is high when large amounts of annotated data are available for supervised training. However, these methods are not suitable when the goal is to transfer knowledge between different domains [44, 52]. Model adaptation from a fully annotated source domains to a target domains has been explored in both semi-supervised and unsupervised settings. Semi-supervised approaches rely on the presence of a small number of annotated target data samples [42, 68]. For example, a weakly supervised signal on the target domain can be obtained using bounding boxes. However, manual data annotation of a small number of images is still a considerable bottleneck.
in the area of medical imaging because only trained professionals can perform this task. For this reason, UDA algorithms are more appealing for healthcare applications.

UDA approaches have explored two main strategies to reduce the domain gap. A large number of works rely on generative adversarial networks (GANs) [24, 69]. The core idea is to use a GAN loss such that data points from both domains can be mapped into a domain-invariant embedding space [21]. To this end, a cross-domain discriminator network is trained to classify whether data embeddings correspond to the source or target domain. An encoder network attempts to fool the discriminator by producing domain agnostic representations for source and target data points. Following this alternating optimization process, a classifier trained using source domain encodings produced by the encoder network would also generalize in the target domain [15, 40]. The weakness of GANs is mode collapse, which requires careful fine-tuning and selection of hyper-parameters in order to be overcome.

Other UDA approaches aim to directly align the distributions of the two domains in a shared embedding space [35, 47, 57]. A shared encoder network is used to generate latent features for both domains. A common latent feature space is achieved by minimizing a suitable probability distance metric between the source and target embeddings [17, 33, 37, 51]. Selecting proper distance metrics has been the major focus of research for these approaches. Optimal transport has been found particularly suitable for deep learning based UDA [13]. We utilize the Sliced Wasserstein Distance (SWD) [35, 46] variant of the optimal transport with similar properties, but which allows for fast gradient based optimization.

The above mentioned sets of approaches have been found helpful in various medical semantic segmentation applications [8, 22, 25, 72]. However, both strategies require direct access to source domain data for computing the loss functions. To relax this requirement, UDA has been recently explored in a source-free setting to address scenarios where the source domain is not directly accessible [30, 53]. Both Kundu et al. [30] and Saltori et al. [53] target image classification, and benefit from generative adversarial learning to generate pseudo-data points that are similar to the source domain data in the absence of actual source samples. While both approaches are suitable for classification problems, extending them to semantic segmentation of medical images is not trivial. First, training models that can generate realistic medical images is considerably more challenging due to importance of fine details. Second, one may argue that if generated images are too similar to real images, the information confidentiality of patients in the training data may still be compromised. Our work is based on using a dramatically different approach. We develop a source-free UDA algorithm that performs the distribution alignment of two domains in an embedding space by using an intermediate internal distribution to relax the need for source data.

3 Problem Formulation

Consider a source domain $D^S = (X^S, Y^S)$ with annotated data and a target domain $D^T = (X^T)$ with unannotated data that despite having different input spaces $X^S$ and $X^T$, e.g., due to using different medical imaging techniques, share the same segmentation map space $Y$, e.g., the same tissue/organ classes. Following the standard UDA pipeline, the goal is to learn a segmentation mapping function for the target domain by transferring knowledge from the source domain. To this end, we must learn a function $f_\theta(\cdot) : \{X^S \cup X^T\} \to \{Y\}$ with learnable parameters $\theta$, e.g., a deep neural network, such that given an input image $x^*$, the function returns a segmentation mask $\hat{y}$ that best approximates the ground truth segmentation mask $y^*$. Given the annotated training dataset $\{(x^i, y^i)_{i=1}^N$ in the source domain, it is straightforward
Figure 1: Proposed method: We first perform supervised training on source MR images. Using the source embeddings we characterize an internal distribution via a GMM distribution in the latent space. We then perform source free adaptation by matching the embedding of the target CT images to the learnt GMM distribution, and fine tuning of the classifier on GMM samples. Finally, we verify the improved performance that our model gains from model adaptation.

to train a segmentation model that generalizes well in the source domain through solving an empirical risk minimization (ERM) problem, i.e., \( \hat{\theta} = \arg\min_\theta \frac{1}{N} \sum_{i=1}^{N} \mathcal{L}(y^s, f_\theta(x^s)) \), where \( \mathcal{L} \) is a proper loss function, e.g., the pixel-wise cross-entropy loss, defined as \( \mathcal{L}_{ce}(y^s, \hat{y}) = -\sum_{i=1}^{W} \sum_{j=1}^{H} \sum_{k=1}^{K} y_{ij}^s \log \hat{y}_{ijk} \). Here, \( K \) denotes the number of segmentation classes, and \( W, H \) represent the width and the height the input images, respectively. Each pixel label \( y_{ij}^s \) will be represented as a one hot vector of size \( K \) and \( \hat{y}_{ij} \) is the prediction vector which assigns a probability weight to each label. Due to the existence of domain gap across the two domains, i.e. discrepancy between the source domain distribution \( p_s(X) \) and the target domain distribution \( p_t(X) \), the source-trained model using ERM may generalize poorly in the target domain. We want to benefit from the information encoded in the target domain unannotated dataset \( \{x_t^M\}_{i=1}^{M} \) to improve the model generalization in the target domain further.

We follow the common strategy of domain alignment in a shared embedding space to adress UDA. Consider our model \( f \) to be a deep convolutional neural network (CNN). Let \( f = \phi \circ \chi \circ \psi \), where \( \psi(\cdot) : \mathbb{R}^{W \times H \times C} \rightarrow \mathbb{R}^{U \times V} \) is a CNN encoder, \( \chi(\cdot) : \mathbb{R}^{U \times V} \rightarrow \mathbb{R}^{W \times H \times K} \) is an up-scaling CNN decoder, and \( \phi(\cdot) : \mathbb{R}^{W \times H \times K} \rightarrow \mathbb{R}^{W \times H \times K} \) is a classification network that takes as inputs latent space representations and assigns label-probability values. We model the shared embedding space as the output space of the sub-network \( \chi \circ \psi(\cdot) \). Solving UDA reduces to ensuring the source and target embedding distributions are aligned in the embedding space. This translates into minimizing the distributional discrepancy between the \( \chi \circ \psi(p_s(\cdot)) \) and \( \chi \circ \psi(p_t(\cdot)) \) distributions. A large group of UDA algorithms \([65, 71]\) select a probability distribution metric \( D(\cdot, \cdot) \), e.g. SWD or KL-divergence, and then use the source and the target domain data points, \( X^S = [x_1^s, \ldots, x_N^s] \) and \( X^T = [x_1^t, \ldots, x_N^t] \), to minimize the loss term \( D(\chi \circ \psi(p_s(\cdot)), \chi \circ \psi(p_t(\cdot))) \) as a regularizer. However, this will constrain the user to have access to the source domain data to compute \( D(\chi \circ \psi(p_s(\cdot)), \chi \circ \psi(p_t(\cdot))) \) that couples the two domains. We provide a solution to align the two domains without sharing the source domain data, that benefits from an intermediate probability distribution.

## 4 Proposed Algorithm

Our proposed approach is based on using the internal distribution \( P_Z \) as a surrogate for the learned distribution of the source domain in the embedding space. Upon training \( f_\theta \) using ERM, the embedding space would become discriminative for the source domain. This means
that the source distribution in the embedding space will be a multimodal distribution, where each mode denotes one of the classes. This distribution can be modeled as a Gaussian Mixture Model (GMM). To develop a source-free UDA algorithm, we can draw random samples from the GMM and instead of relying on the source data, align the target domain distribution with the internal distribution in the embedding space. In other words, we estimate the term $D(\chi \circ \psi(p_s^t(\cdot)), \chi \circ \psi(p_t^t(\cdot)))$ with $D(\mathcal{P}_Z(\cdot), \chi \circ \psi(p_t^t(\cdot)))$ which does not depend on source samples. We use SWD as the distribution metric for minimizing the domain discrepancy. A visual concept-level description for our approach is presented in Figure 1.

The intermediate distribution. The function $\psi \circ \chi$ transforms the input distribution $p_s^t(\cdot)$ to the internal distribution $\mathcal{P}_Z(\cdot) = \chi \circ \psi(p_s^t(\cdot))$ based on which the classifier $\phi$ assigns labels. This distribution will have $K$ modes. Our idea is to approximate $\mathcal{P}_Z(\cdot)$ via a GMM with $\omega \times K$ components, with $\omega$ components for each of the $K$ semantic classes:

$$\mathcal{P}_Z(z) = \sum_{c=1}^{\omega K} \alpha_c p_c(z) = \sum_{c=1}^{\omega K} \alpha_c N(z|\mu_c, \Sigma_c),$$

where $\alpha_c$ represents the mixture probabilities, $\mu_c$ represents the mean of the Gaussian $c$, and $\Sigma_c$ is the covariance matrix of the $c^{th}$ component. Under the above representation, each semantic class $k \in \{1...K\}$ will be represented by $\omega$ components: $(k-1)\omega + 1...k \omega$. When the network $f$ is trained on the source domain, we can estimate the GMM parameters class-conditionally from the latent features obtained from the source training samples $\{\phi(\chi(x^s))_{ij}, y^s_j\}$. Once class specific latent embeddings are computed via access to the labels $Y^s$, we estimate the corresponding $\omega$ components using the EM algorithm.

Sample selection. To improve class separations in the internal distribution $\mathcal{P}_Z$, we only use high-confidence samples in each class for estimating parameters of $p_c(\cdot)$. We use a confidence threshold parameter $\rho$, and discard all samples for which the classifier confidence on its prediction $p_{ij}$ is strictly less than $\rho$. This step helps cancel out class outliers. Let $\mathcal{S}_p = \{(x^s_{ij}, y^s_{ij})|\max\phi(\chi(x^s_{ij})) > \rho\}$ be the source data pixels on which the classifier $\phi$ assigns confidence greater than $\rho$. Also, let $\mathcal{S}_{p,k} = \{(x,y)|(x,y) \in \mathcal{S}_p, y = k\}$. Then, for each class $k$ we generate empirical estimates for the $\omega$ components defined by triplets $(\hat{\alpha}_{\omega(k-1)+1}, \hat{\mu}_{\omega(k-1)+1}, \hat{\Sigma}_{\omega(k-1)+1}) \cdots (\hat{\alpha}_{\omega k}, \hat{\mu}_{\omega k}, \hat{\Sigma}_{\omega k})$ by applying EM to $\mathcal{S}_{p,k}$ data points.

The adaptation loss. Given the estimated internal distribution parameters $\hat{\alpha}, \hat{\mu}, \hat{\Sigma}$, we can perform domain alignment. Adapting the model should lead to the target latent distribution $\chi(\psi(p_t^t(\chi)))$ matching the distribution $\mathcal{P}_Z$ in the embedding space. To this end, we can generate a pseudo-dataset $D^p = (Z^p, Y^p)$ by drawing samples from the GMM and aligning $\chi(\psi(X^T))$ with $Z^p$ to reduce the domain gap. The alignment loss can then be formalized as:

$$\mathcal{L}_{adapt} = \mathcal{L}_{ce}(\phi(Z^p), Y^p) + \lambda \mathcal{D}(\chi(\psi(X^T)), Z^p)$$

(1)

The first term in Eq. 1 involves fine-tuning the classifier on samples from the pseudo-dataset $(Z^p, Y^p)$ to ensure that it would continue to generalize well. The second term enforces the distributional alignment. Since the source samples are not used in Eq. 1, data confidentiality will also be preserved. The last ingredient for our approach is selection of the distance metric $\mathcal{D}(\cdot, \cdot)$. We used SWD for this purpose. The pseudocode for our approach, called Source Free semantic Segmentation (SFS), is presented in Alg. 1.
5 Experimental Validation

5.1 Datasets

Multi-Modality Whole Heart Segmentation Dataset (MMWHS) [77]: this dataset consists of multi-modality whole heart images obtained on different imaging devices at different imaging sites. Segmentation maps are provided for 20 MRI 3D heart images and 20 CT 3D heart images which have domain gap. Following the UDA setup, we use the MRI images as the source domain and CT images as the target domain. We perform UDA with respect to four of the available segmentation classes: ascending aorta (AA), left ventricle blood cavity (LVC), left atrium blood cavity (LAC), myocardium of the left ventricle (MYO).

We will use the same experimental setup and parsed dataset used by Dou et al. [15] for fair comparison. For the MRI source domain we use augmented samples from 16 MRI 3D instances. The target domain consists of augmented samples from of 14 3D CT images, and we report results on 4 CT instances, as proposed by Chen et al. [6]. Each 3D segmentation map used for assessing test performance is normalized to have zero mean and unit variance.

CHAOS MR → Multi-Atlas Labeling Beyond the Cranial Vault: the second domain adaptation task consists of data frames from two different dataset. As source domain we, consider the the 2019 CHAOS MR dataset [26], previously used in the 2019 CHAOS Grad Challenge. The dataset consists of both MR and CT scans with segmentation maps for the following abdominal organs: liver, right kidney, left kidney and spleen. Similar to [6] we use the T2-SPIR MR images as the source domain. Each scan is centered to zero mean and unit variance, and values more than three standard deviations away from the mean are clipped. In total, we obtain 20 MR scans, 16 of which we use for training and 4 for validation. The target domain is represented by the dataset which was presented in the Multi-Atlas Labeling Beyond the Cranial Vault MICCAI 2015 Challenge [32]. We utilize the 30 CT scans in the training set which are provided segmentation maps, and use 24 for adaptation and 6 for evaluating generalization performance. The value range in the CT scans was first clipped to $[-125, 275]$ HU following literature [32]. The images were re-sampled to an axial view size of $256 \times 256$. Background was then cropped such that the distance between any labeled pixel and the image borders is at least 30 pixels, and scans were again resized to $256 \times 256$. Finally, each 3D scan was normalized independently to zero mean and unit variance, and values more than three standard deviation from the mean were clipped. Data augmentation was performed on both the training MR and training CT instances using: (1) random rotations of up to 20 degrees, (2) negating pixel values, (3) adding random Gaussian noise, (4) random cropping.

Both of the above problems involve 3D scans. However our network encoder architecture receives 2D images at its input, where each image consists of three channels. To circumvent this discrepancy, we follow the frame-by-frame processing methodology by Chen et al. [6]. We convert higher dimensional features into 2D images by creating images from groups of three consecutive scan slices, and using them as labels for the segmentation map of the middle slice. Implementation details re included in the Appendix.

Algorithm 1 SFS ($\lambda, \rho, \omega$)

1: Initial Training:
2: Input: Source dataset $D^S = (X^S, Y^S)$,
3: Training on Source Domain:
4: $\hat{\theta}_0 = \arg \min_{\theta} \sum_i \ell(f_\theta(x_i^S), y_i^S)$
5: Internal Distribution Estimation:
6: Set $\rho = 0.97$, compute $S_{p,k}$, and estimate $\hat{\alpha}_j, \hat{\mu}_j, \hat{\Sigma}_j$ class conditionally via EM
7: Model Adaptation:
8: Input: Target dataset $D^T = (X^T)$
9: Pseudo-Dataset Generation:
10: $D^P = (Z^P, Y^P) = ([z^p_1, \ldots, z^p_N], [y^p_1, \ldots, y^p_N])$, where: $z^p_i \sim P_Z(z), 1 \leq i \leq N_p$
11: for $itr = 1 \rightarrow ITR$ do
12: Draw batches from $D^T$ and $D^P$
13: Update the model by solving Eq. (1)
14: end for
5.2 Evaluation Methodology

Following the medical image segmentation literature, we use two main metrics for evaluation: dice coefficient and average symmetric surface distance (ASSD). The Dice coefficient is a popular choice in medical image analysis works and measures semantic segmentation quality [6, 9, 74]. It is used for direct evaluation of segmentation accuracy. The ASSD is a metric which has been used [6, 9, 73] to assess the quality of borders of predicted segmentation maps which are important for diagnosis. A good segmentation will have a large Dice coefficient and low ASSD value, the desirability of a result being application dependant.

We compare our approach to other state-of-the-art techniques developed for unsupervised medical image segmentation. We compare against adversarial approaches PnP-AdaNet [16], SynSeg-Net [23], AdaOutput [22], CycleGAN [76], CyCADA [21], SIFA [8], ARL-GAN [11], DSFN [78], SASAN [24], DSAN [19]. These works are recent methods for semantic segmentation that serve as upper bounds for our approach, as we do not process the source domain data directly. We reiterate the advantage of our method is to preserve the confidentiality of patient data, and we do not claim best performance. We also compare against GenAdapt [31], a SOTA street semantic segmentation method that is not tuned for the medical field. Finally, we also evaluate our model against AdaEnt [2] and AdaMI [3], two recent source-free approaches designed for medical semantic segmentation, and observe our methods outperforms both these techniques. Our code is available as a supplementary material.

5.3 Quantitative and Qualitative Results

Tables 1 and 2 summarize the segmentation performance for our method along with other baselines. As mentioned, when compared to other UDA approaches our method has the additional benefit of not violating data confidentiality on the source and target. This means most other approaches should serve as upper bounds for our algorithm, as they do not enforce restrictions for jointly accessing source and target data. We also compare against a recent street semantic segmentation algorithm [31] to verify whether real world adaptation approaches are at a disadvantage due to the specificity of medical data. We observe this approach has indeed lowest performance out of the considered methods. On the MMWHS dataset we achieve SOTA performance on class AA. We obtain the highest Dice score out of the considered methods, due to our high average performance on all classes. The ASSD score is competitive with other approaches, the best such score being observed for GAN based methods. This shows our domain alignment approach successfully maps each class in the target embedding to its corresponding vicinity using the internal distribution. For the abdominal task we observe similar trends. We achieve SOTA performance on class Liver, and competitive performance on the other classes. These results suggest that our method offers the possibility of domain adaptation with competitive performance.

In Figure 5, we present the improvement in segmentation on CT scans from both datasets. In both cases, the supervised models are able to obtain a near perfect visual similarity to the ground truth segmentation which represent the upper-bound performance. Post-adaptation quality of the segmentation maps becomes much closer to the the supervised regime from a visual perspective. We observe fine details on image borders need more improvement in images 2, 5, 6, 10. This is in line with the observed ASSD performance. Overall, our approach offers significant gains with respect to the Dice coefficient, which directly measures the segmentation accuracy. The improvement in surface distance is also consistent, however best ASSD performance is observed for [11], a method with joint access to source data. Still, our algorithm has the advantage of also maintaining data confidentiality during adaptation.
Table 1: Segmentation performance comparison for the Cardiac MR → CT adaptation task. Starred methods perform source-free adaptation. Bolded cells show best performance.

| Method      | Liver | R.Kidney | L.Kidney | Spleen | Average | Liver | R.Kidney | L.Kidney | Spleen | Average |
|-------------|-------|----------|----------|--------|---------|-------|----------|----------|--------|---------|
| Source-Only | 73.1  | 47.3     | 57.3     | 55.1   | 58.2    | 2.9   | 5.6      | 7.7      | 7.4    | 5.9     |
| Supervised  | 94.2  | 87.2     | 88.9     | 89.1   | 89.8    | 1.2   | 1.2      | 1.1      | 1.7    | 1.7     |
| SynSeg-Net  | 83.0  | 82.1     | 72.7     | 81.0   | 80.2    | 2.2   | 1.3      | 2.1      | 2.0    | 1.9     |
| AdaOutput   | 85.4  | 79.7     | 79.7     | 81.7   | 81.6    | 1.7   | 1.2      | 1.8      | 1.6    | 1.6     |
| CycleGAN    | 83.4  | 79.3     | 79.4     | 77.3   | 79.9    | 1.8   | 1.3      | 1.2      | 1.9    | 1.6     |
| CyCADA      | 84.5  | 78.6     | 80.3     | 76.9   | 80.1    | 2.6   | 1.4      | 1.3      | 1.9    | 1.8     |
| SIFA        | 88.0  | 83.3     | 80.9     | 82.6   | 83.7    | 1.2   | 1.0      | 1.5      | 1.6    | 1.3     |
| SFS’        | **88.3** | 73.7     | 80.7     | 81.6   | 81.1    | 2.4   | 4.1      | 3.5      | 2.7    | 3.2     |

Table 2: Segmentation performance comparison for the Abdominal MR → CT task.

5.4 Ablation Studies and Empirical Analysis

We empirically demonstrate why our algorithm works by screening changes in the latent embedding before and after adaptation. To visualize the embeddings, we use UMAP [41] to reduce the high-dimensional embeddings to 2D. Figures 2 and 3 showcase the impact of our algorithm on the latent distribution of the two datasets. In Figure 2(a), we record the latent embedding of the GMM distribution that is learned on the cardiac MR embeddings. Figure 2(b) exemplifies the distribution of the target CT samples before adaptation. We see from Table 1 that the source-trained model is able to achieve some level of pre-adaptation class separation which is confirmed in Figure 2(b). In Figure 2(c) we observe that this overlap is reduced after adaptation. We also observe that the latent embedding of the target CT samples is shifted towards the internal distribution, making the source-trained classifier generalizable. We repeat the same analysis for the organ segmentation dataset, and observe a similar outcome. We conclude that our intuition is confirmed, and the algorithm mitigates domain shift by performing distribution matching in the latent embedding space.

We also investigate the impact of the \( \rho \) parameter on our internal distribution. In Figure 4 we present the UMAP visualization for the learnt GMM embeddings for three different values of \( \rho \). We observe that while some classes will be separated for \( \rho = 0 \), using high confidence samples to learn the GMM will yield higher separability in the internal distribution. We observe our algorithm is robust when \( \rho \) is close to 1, hence our choice of \( \rho = .97 \).
Figure 2: Indirect distribution matching in the embedding space: (a) GMM samples approximating the MMWHS MR latent distribution, (b) CT latent embedding prior to adaptation (c) CT latent embedding post domain alignment. Colors correspond to: AA, LAC, LVC, MYO.

Figure 3: Indirect distribution matching: (a) GMM samples approximating the CHAOS MR latent distribution, (b) Multi-Atlas CT embedding prior to adaptation (c) Multi-Atlas CT embedding post adaptation. Colors correspond to: liver, right kidney, left kidney, spleen.

Figure 4: Learnt Gaussian embeddings on the cardiac dataset for different $\rho$. Ignore

|     | Ignore | MYO | LAC | LVC | AA  |
|-----|--------|-----|-----|-----|-----|
| Ignore | 97.3 99.3 99.3 | 1.5 20.3 70.0 | 0.2 80.2 14.8 | 0.9 6.2 76.1 | 0.2 43.8 51.7 |
| MYO | 13.2 10.4 89.5 | 81.6 72.2 72.2 | 0.1 52.7 0.4 | 5.2 44.6 54.1 | 0.0 0.0 0.0 |
| LAC | 15.1 45.4 46.3 | 2.5 2.6 79.7 | 76.1 88.4 88.4 | 5.9 7.4 87.4 | 0.4 5.8 77.0 |
| LVC | 0.6 67.7 2.3 | 16.5 33.4 66.3 | 0.2 83.8 13.0 | 82.7 92.4 92.4 | 0.0 93.3 0.0 |
| AA | 18.5 7.8 90.9 | 0.0 0.0 43.7 | 1.3 5.7 62.1 | 0.1 0.0 12.9 | 80.1 91.2 91.2 |

Table 3: Percentage of shift in pixel labels during adaptation for the cardiac dataset. A cell $(i, j)$ in the table has three values. The first value represents the percentage of pixels labeled $i$ that are labeled $j$ after adaptation. The second value represents the percentage of switching pixels whose true label is $i$ - lower is better. The third value represents the percentage of switching pixels whose true label is $j$ - higher is better. Bolded cells denote label shift where more than 1% of pixels migrate from $i$ to $j$.

Table 4: Percentage of shift in pixel labels during adaptation for the abdominal organ dataset. The same methodology as in Table 3 is used.

The outcome of pixel label shift is analyzed in Tables 3 and 4. In Table 3 we observe that for the cardiac dataset there exists significant inter-class label transfer, for approximately 20% of pixels, evenly distributed across classes. We see the majority of these shifts leading to an improvement in labeling accuracy, including all shifts where at least 1% of labels mi-
grate, which is in line with our other reported results. These findings also corroborate with our observed embeddings. We can see from Table 3 that during adaptation there is significant label migration between LVC and MYO, and this can be observed in the increased separation between the two classes in Figures 2(b) and 2(c). For the abdominal organ dataset we observe significantly less label shift between classes, with most of the activity involving previously labeled pixels being correctly le-labeled as Ignore after adaptation, or pixels initially in Ignore being correctly le-labeled to their appropriate class.

We also perform an ablative experiment for the $\omega$ parameter using the the cardiac dataset in Table 5. We observe a large increase in performance when using more than one component per class. However, this benefit decreases as more components are employed. We observe using more than 2 components increases the Dice score, and more than a 30% drop in ASSD. We conclude a larger number of class components can offer a more expressive approximation of the source distribution, leading to improvements for segmentation accuracy and organ border quality. In our study we choose $\omega = 3$ to balance performance and complexity.

Full experimental setup and additional results are provided in the appendix.

| $\omega$-SFS | Dice | Average Symmetric Surface Distance | $\omega$-SFS | Dice | Average Symmetric Surface Distance |
|--------------|------|----------------------------------|--------------|------|----------------------------------|
| $1$-SFS      | 86.2 | 83.5 75.4 70.9 | Average | 11.1 | 5.0 10.8 3.6 | Average | 9.8 |
| $3$-SFS      | 88.0 | 83.7 81.0 72.5 | 81.3 | 6.3 | 7.2 4.7 | 6.1 |
| $5$-SFS      | 88.0 | 83.8 81.9 73.3 | 81.7 | 6.2 | 7.4 4.8 | 5.7 | 6.0 |
| $7$-SFS      | 86.8 | 84.8 82.0 73.5 | 81.8 | 4.8 | 7.2 4.4 | 5.6 | 5.9 |

Table 5: Segmentation performance versus $\omega$ for the Cardiac MR $\rightarrow$ CT adaptation task.

Figure 5: Segmentation maps of CT samples. The first five columns correspond to cardiac images, and last five correspond to abdominal images. From top to bottom: gray-scale CT images, source-only predictions, post-adaptation predictions, supervised predictions on the CT data, ground truth.

6 Conclusion

We developed a novel UDA algorithm for semantic segmentation of confidential medical data. Our idea is based on estimating the source internal distribution via a GMM and then using it to align source and target domains indirectly. We provided a empirical analysis to demonstrate why our method is effective and it leads to competitive performance on two real-world datasets when compared to state of the art approaches in medical semantic segmentation that require joint access to source and target data for adaptation.
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7 Appendix

7.1 Experimental Setup

We use the same network architecture on both the cardiac and organ image segmentation UDA task. We use a DeepLabV3 \cite{deeplabv3} feature extractor with a VGG16 backbone \cite{vgg16}, followed by a one layer classifier.

We train the network on the supervised source samples with a training schedule of 30,000 epochs repeated 3 times. The optimizer of choice is Adam with learning rate $1e^{-4}$, $\epsilon = 1e^{-6}$ and decay of $1e^{-6}$. We use the standard pixel-wise cross entropy loss, and batch size of 16. For the abdominal organ segmentation dataset, we observed better performance by using a weighted cross entropy loss.

We learn the empirical internal distribution using a parameter $\rho = .97$. We observed good separability in the latent distribution for $\rho \geq .9$.

We use $\omega = 3$ components per each of the $K$ classes, though as seen in Table 5, a larger $\omega$ could potentially lead to further performance gains. $\omega = 3$ strikes a balance between the complexity of the GMM model and realized performance.

Finally, when performing adaptation, we performed 35,000 epochs of training, with a batch size of 32. We again use an Adam optimizer with a learning rate of $5e^{-5}$, $\epsilon = 1e^{-1}$ and decay of $1e^{-6}$. Due to GPU memory constraints leading to a limited amount of image slices per batch, and therefore a large label distribution shifts between target batches, when sampling from the learnt GMMs we approximate the target distribution via the batch label distribution.

Experiments were done on a NVIDIA RTX 3090 GPU. Code is provided in the supplementary material section of this submission, and will be made freely available online at a later date.

7.2 Additional Ablation Studies

We further empirically analyze different components of our approach to demonstrate their effectiveness.

**Fine-tuning the classifier.** As we discussed in the main body of the paper, after learning an internal distribution characterizing the source embeddings, we align the target embeddings to this distribution by minimizing Sliced Wasserstein Distance. In addition, we also further train the classifier on samples from this distribution to account for differences to the original source embedding distribution. We next discuss the benefit of fine tuning the classifier, based on the results in Table 6.

| Metric | Fine-Tuned Classifier | Source Domain Classifier |
|--------|-----------------------|--------------------------|
| Dice   | 81.3                  | 80.9                     |
| ASSD   | 6.1                   | 7.35                     |

Table 6: Target performance on the MMWHS adaptation task of our method with and without fine tuning the classifier on samples from the internal distribution. Bolded values indicate best performance.

Given the learnt empirical means and covariances for the internal distribution, we compare the performance after target domain adaptation between a model that fine tunes the classifier and a model that does not update the classifier after source training. As expected,
fine tuning the classifier offers a prediction boost, even if the difference is not a significant one. The internal distribution is meant to encourage the target embeddings to share a similar latent space with the source embeddings, and fine tuning the classifier accounts for the distribution shift between the source embeddings and learnt internal distribution.

**Filter visualization.** We also investigate the information encoded in the convolutional filters before and after adaptation. Based on our results, we expect network filters to retain most of their structure from source training, and not alter this structure too much during distribution matching. We exemplify this in Figure 6. We record the visual characteristics of the network filters after the first two convolutional layers and the first four convolutional layers. We observe filters appear visually similar before and after adaptation, signifying image structural features learnt by the network do not undergo significant change, even though changes in filter values can be observed under the *Difference* columns.

Figure 6: Filter maps of a cardiac CT image before and after model adaptation. In the case of filter differences in absolute value, dark grey symbolizes lower values, while light gray symbolizes higher values.