Chapter

Hysteresis Behavior of Pre-Strained Shape Memory Alloy Wires Subject to Cyclic Loadings: An Experimental Investigation

Shahin Zareie and Abolghassem Zabihollah

Abstract

Shape memory alloys (SMAs) are a class of smart materials with the ability to recover their initial shape after releasing the applied load and experiencing a relatively large amount of strain. However, sequential loading and unloading which is an unavoidable issue in many applications significantly reduces the strain recovery of SMA wires. In the present work, experimental tests have been performed to study the pre-strain effect of SMA wires on hysteresis behavior of SMA under cyclic loadings. The effects of cyclic loading on austenite and martensite properties have been investigated. SMA wires with diameter of 1.5 mm and length of 560 mm subjected to about 1000 cycles show about 3 mm residual deformation, which is approximately equal to 0.5% residual strain. It is observed that applying 1.7% pre-strain on the SMA wire fully eliminates the residual strain due to cyclic loading.

Keywords: shape memory alloy, cyclic loading, pre-strained, residual deformation

1. Introduction

Stability and failure control of structures are of the major challenges for civil structures in which the loading conditions are cyclic in nature, including harbor and offshore structures. In the past decades, a variety of active control mechanisms have been developed to ensure the stability of such structures [1]. However, active control mechanisms are relatively complex, requiring expensive and professional maintenance which are not always accessible. Therefore, for many structures, passive stability control mechanisms are preferred. Shape memory alloys (SMAs), due to their unique ability to recover their initial shape after releasing the applied load, are promising materials for energy absorption and ensuring the stability of structure under relatively large strain [2–7]. However, it is understood that the cyclic loading may highly influence the strain recovery property, superelasticity, of SMAs [8]. This phenomenon has been widely investigated by researchers in smart structure communities.

Zhang et al. [9] developed a low cycle fatigue criterion for superelasticity of SMAs considering thermomechanical coupling. They concluded that increasing strain rate decreases the fatigue lifetime in SMAs. A micromechanical model to describe the cyclic deformation of polycrystalline NiTi under different...
thermomechanical conditions has been proposed by [10]. Wang et al. [11] proposed a novel structural building element integrated with SMA material to show the capability of SMA-based element in re-centering and energy dissipation of the structure after severe displacement.

Chemisky et al. [12] proposed an analytical model to describe the effects of cyclic loading at high temperature on SMAs behavior. Recently, remarkable researches have been performed to study the different parameters related to cyclic loadings on SMAs’ behavior. Kan et al. [13] studied the effect of strain rate on uniaxial deformation of NiTi. Soul et al. [14] investigated the effect of loading frequency on the damping capacity of NiTi wires and concluded that loading frequency above 0.01 Hz significantly reduces the damping capacity of SMA wires. Des Roches et al. [15] evaluated the change in superelasticity of bar and wires made of NiTi under cyclic loading.

The present work aims to investigate the effects of pre-strained SMA wires under cyclic loading conditions on force-displacement behavior, particularly austenite and martensite phases, of SMAs. Experimental tests have been conducted to study the effect of the number of cycles, frequency of loading, and the pre-straining on hysteresis behavior of SMA wires under cyclic loadings.

2. Modeling superelasticity effect of SMA

When the temperature is equal to or greater than the austenitic finish temperature ($T \geq A_f$), SMA materials exhibit the superelasticity effect. Figure 1 shows the stress-strain curve for loading and unloading of an SMA material. In the loading phase, there are two parts: linear and plastic, whereas in the unloading process, the material exhibits three portions, huge stress reduction with negligible strain reduction, huge strain reduction with a small amount of stress, and finally linear stress-strain reduction. It is noted that the area under the stress-strain curve describes the energy dissipation property of the SMA when loading and unloading. For an SMA rod with cross section ($A$) subjected to the axial loading ($F$), the stress
is given by \( \sigma = F/A \). Neglecting thermal expansion, the stress-strain of the SMA rod is computed as [16, 17]:

\[
\sigma - \sigma_0 = E(\varepsilon - \varepsilon_0) + \Omega(\xi - \xi_0)
\]

(1)

where \( 0 \leq \xi \leq 1 \) indicates martensite fraction which is equal to zero for fully austenite phase and 1 for fully martensite. The term \( \Omega \) is the transformation coefficient. Considering initial state as \( \sigma_0 = \varepsilon_0 = 0, \xi_0 = 0 \) and noting that after full phase transformation the material returns to zero stress, the transformation coefficient may be defined as a function of residual strain, \( \Omega = E\varepsilon_r \). Therefore, the stress-strain relations for SMA can be expressed as:

\[
\sigma - \sigma_0 = E(\varepsilon - \varepsilon_0) + \varepsilon_r E(\xi - \xi_0)
\]

(2)

Eq. (2) can be modified for each region, for example, in the linear elastic region where the material is in full austenite phase (\( \xi = 0 \)); Eq. (2) is given as:

\[
\sigma = \varepsilon_r E
\]

(3)

where \( E_A \) indicates the modulus of elasticity in austenite phase; similarly, for linear unloading stage where the material is in full martensite phase, modulus of elasticity is defined by \( E_M \). For other regions, modulus of elasticity is a combination of \( E_A \) and \( E_M \) as the following [16, 17]:

\[
E = E_A + (E_M - E_A)\xi
\]

(4)

Further unloading beyond this point produces a linear elastic behavior to zero stress-strain. For further description on stress-strain relationships for superelasticity effect, one may refer to the book written by [16]. However, one may note that in the above expression, the effect of the number of loading/unloading cycles and pre-straining is not taken into consideration. The following sections provide a thorough study, particularly experimentally, on the effects of cyclic loading and pre-straining on stress-strain behavior of SMA materials.

3. Experimental tests

Experimental tests have been conducted using a universal testing machine—MTS model 370.5 with 500 kN loading capacity, 150 mm dynamic stroke, and 0.1–1 Hz loading frequency as shown in Figure 2. The SMA wire specimen of 560 mm length with 1.5 mm diameter made of NiTi has been subjected to cyclic tensile loadings. The material properties of NiTi wire, manufactured by Confluent Medical Technologies Company, are given in Table 1. Due to the small diameter of the specimen, each plate is clamped by the top and bottom grippers of the MTS loading machine, as shown in Figure 3. Loading frequencies, initial tensile load, loading rates, and the number of cycles have been predefined in the MTS machine for each test.

3.1 Single cycle loading and unloading test

In order to determine the force-displacement response curve for SMA specimen, a NiTi wire described above has been tested at room temperature with a quasi-static loading/unloading, with the period of 20 s and maximum amplitude 12 mm, as
Figure 2.
The MTS loading frame machine and its accessories.

| Physical properties                          | Value       |
|----------------------------------------------|-------------|
| Melting point (°C)                           | 1310        |
| Density (g/cm³)                              | 6.5         |
| Electrical resistivity (μ ohm·cm)            | 82          |
| Modulus of elasticity (GPa)                  | 41–75       |
| Coefficient of thermal expansion (/°C)       | $11 \times 10^{-6}$ |
| Ultimate tensile strength (MPa)              | ~1070       |
| Total elongation                             | ~10%        |
| Straight length (mm)                         | 560         |
| Diameter (mm)                                | 1.5         |

Table 1.
The properties of NiTi shape memory alloy.

Figure 3.
The experimental setup for gripping the SMA specimen.

presented in Figure 4. Then, the test specimen is subjected to a cyclic load with 1000 cycles in which the period and maximum amplitude for the first cycle is 1.4 s and 20 mm, correspondingly, as shown in Figure 5. After completing 1000 cycles, the specimen is subjected again to the quasi-static load given in Figure 4. The force-displacement behavior of the specimen under the first quasi-static load and after
1000 load cycles are shown in Figure 6, in which 0 cycle stands for the quasi-static loading described in Figure 4. After 1000 load cycles, two major impacts on the force-displacement curve of SMA are realized, a significant reduction on hysteresis which, in turn, results in reduction in energy absorption, and reduction in material properties, $E_A$ and $E_M$. Reduction in material properties is mainly due to the degradation phenomena of SMA. The effect of cyclic loading/unloading on material properties, $E_A$ and $E_M$, are presented as a correction factor of the ratio of $E$ after 1000 cycle ($E_{1000}$) and $E$ when the specimen is subjected to a single quasi-static load ($E_0$), in Figure 6. After 1000 cycles, $E_A$ shows 18% reduction, whereas $E_M$ 33% compared to the initial single quasi-static loading condition.
3.2 Effect of pre-straining on SMA properties

Long-term stability and performance of civil structures under dynamic loadings is an essential feature for many applications. Therefore, structural designers do not tolerate the change in structural strength and stability. As it was realized in the previous section, cyclic load results in a significant reduction in material properties and, in turn, a reduction in the stability and loading characteristics of SMA-based structural elements.

In order to mitigate the negative effect of cyclic loading on SMA-based elements, 10 mm initial displacement is applied to the SMA wire, which is far beyond the elastic displacement region, and 10 mm is approximately equal to 1.7% pre-strain. The hysteresis response of 1.7% pre-strained SMA wire subjected to the loading protocol, as presented in Figure 5, after 1000 cycles, is given in Figure 7. Comparison of Figure 7 and Figure 6 exhibits that pre-straining SMA eliminates the residual deformation occurred after 1000 cyclic load/unloading.

Figure 8 provides the comparison between $E_A$ and $E_M$ of the specimen after applying 1000 cyclic loads. It is noted that pre-straining improves the value of $E_A$ from 82% at 0% pre-strain to 52% at 1.7% pre-straining the specimen. However, 1.7% pre-straining completely return the value of $E_M$ from 67% at 0% to its initial state.

![Figure 7](image1.png)

*Figure 7.* The hysteresis response of 1.7% pre-strain specimen after applied 1000 cycles.

![Figure 8](image2.png)

*Figure 8.* The effect of applied cyclic loading on characteristics of 0 and 1.7% pre-strain specimen.
3.3 Effect of pre-straining and sequentially increasing load on SMA properties

Sequentially increasing loadings is a common loading profile for many civil applications including offshore structures, requiring a thorough understanding of the response of structures under such loading profile. In this section, two specimens are exposed to a sequentially increasing quasi-static loading protocol as presented in Figure 9. It composes of four cycles with 20 s period and arbitrary amplitude of 11.61 mm, (called loading sequence (LS) 1), 13.58 mm (called loading sequence (LS) 2), 17.51 mm (called loading sequence (LS) 3), and 19.48 mm (called loading sequence (LS) 4), respectively. Two parameters, namely, $E_A$ and $E_M$, have been studied again under this loading protocol. Then, the loading profile is repeated for 1000 cycles, and the response of the specimens is recorded. Similar to the constant loading profile, it is observed that cyclic load leads to a significant reduction in material properties, $E_A$ and $E_M$. In another experiment, the specimens are subjected to 1.7% pre-straining where it revealed a significant improvement in the material properties. As shown in Figure 10, applying a value of 1.7%, pre-strain changes the value of the correction factor $E_{A1000}/E_A$ from 62% (for the first period) to 81% (for the fourth period) to 52 and 72%, correspondingly. In a similar observation, applying a value of 1.7%, pre-straining changes the value of the correction factor $E_{M1000}/E_M$ from 67 to 54%.

Figure 9.
The loading protocol for 0 and 1.7% pre-strain specimen.

Figure 10.
The effect of cyclic loading on $E_A$ of 0 and 1.7% pre-strain specimen.
4. Correction factor for stress-strain of SMA under cyclic loadings

Close study of force-displacement curves for SMA specimen subjected to cyclic loading, and pre-straining reveals that the number of cycles and pre-straining significantly influences the predetermined stress-strain behavior of SMA-based structural elements. In many applications the structure undergoes dynamic loadings, requiring an accurate yet practical estimation of the effect of loading conditions, on the performance and functionality of the structure for long-term usage. According to the present experimental results, practical correction factors are introduced to estimate the effects of cyclic. According to the present experimental results, it is realized that the change in $E_A$ and $E_M$ is a function of correction factors relating cyclic loading, pre-straining, and initial material properties as the following:

$$E_A'' = f(\alpha, \beta, E_A), E_M'' = f(\alpha', \beta', E_M)$$ (5)

where $\alpha$ and $\alpha'$ are the correction factors relating $E_{A1000}/E_{A0}$ and $E_{M1000}/E_{M0}$. Similarly $\beta$ and $\beta'$ are correction factors relating $E_{A1000}$ at 1.7% pre-straining / $E_{A3000}$ at 0% pre-straining and $E_{M1000}$ at 1.7% pre-straining / $E_{M1000}$ at 0% pre-straining. The terms $E_A''$ and $E_M''$ indicate corrected value for $E_A$ and $E_M$ as a result of cyclic loading and pre-straining. Accordingly, the functions relating $E_A''$ to $E_A$ and $E_M''$ to $E_M$ can be estimated as:

$$E_A'' = \alpha \beta E_A, E_M'' = \alpha' \beta' E_M$$ (6)

The correction factors, $\alpha \beta$ and $\alpha' \beta'$ are presented in Figures 10 and 11. The values for $\alpha$ and $\alpha'$ are given in Figure 12.

As observed in the conventional specimen (0% pre-straining), $\beta$ and $\beta'$ are assumed 1. Hence, Eq. (6) is now modified to:

$$E_A'' = \alpha E_A, E_M'' = \alpha' E_M$$ (7)

where $\alpha = 0.6 - 0.81$ and $\alpha' = 0.6 - 1.2$.

In the case of applied 1.7% pre-straining, coefficients in Eq. (6) can be calculated by $\alpha \beta = 0.45-0.8$ and $\alpha' \beta' = 0.56 - 0.98$.
Considering the effects of cyclic loading and pre-straining on stress-strain behavior of SMA wires, Figure 13(a) is now modified to Figure 13(b), where one may realize a significant reduction in critical stress-strain points as well as changes in residual strain after cyclic loading.

Figure 12.
The effect of applied cyclic loading on EA and EM.

Figure 13.
The effect of cyclic loading (a) 0% pre-strained SMA (b) 1.7% pre-strained SMA on EA and EM.
5. Conclusions

The effects of cyclic loading and pre-straining on stress-strain behavior of SMA wires have been investigated. Several experimental tests have been conducted to study the effects of the number of cycles and pre-straining on strain recovery and modulus of elasticity of SMA wires. Correction factors have been provided to encounter the effects of cyclic loads and pre-straining on stress-strain behavior of SMA wires. It is observed that cyclic loading may lead to huge residual strain and reduces the strain recovery feature of SMA. However, pre-straining SMA for only 1.7% significantly improves the reduction in strain recovery of SMA as a result of cyclic loading.

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