Superconducting properties of Rh₃In₄S₄ single crystals

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The synthesis and crystallographic, thermodynamic and transport properties of single crystalline Rh₃In₄S₄ were studied. The resistivity, magnetization and specific heat measurements all clearly indicate bulk superconductivity with a critical temperature, Tc ~ 2.25 K. The Sommerfeld coefficient γ and the Debye temperature (θD) were found to be 34 mJ mol⁻¹ K⁻² and 217 K respectively. The observed specific heat jump, ΔC/γTc = 1.66, is larger than the expected BCS weak coupling value of 1.43. Ginzburg-Landau (GL) ratio of the low temperature GL-penetration depth, λGL≈5750Å, to the GL-coherence length, ξGL≈94Å, is large: κ ~ 60. Furthermore, we observed a peak effect in the resistivity measurement as a function of both temperature and magnetic field.

I. INTRODUCTION

Transition-metal chalcogenides show diverse physical states such as charge density wave1–4, superconductivity5–9, ferromagnetism10,11 and semi-conducting behavior.12,13 The ability to change their properties by doping5,14,15 or pressure16,17 has recently attracted great attention. Of specific interest, some members of metal-rich chalcogenides10,18–20, A₂M₄X₂ (A=Sn,Pb,In,Tl and Bi; M=Co,Ni,Rh and Pd; X=S and Se) are superconducting at low temperatures9,21,22. Interestingly Bi₂Rh₂Se₂23 is a superconductor that shows a possible high-temperature (~240 K) charge density wave transition. In contrast, the isostructural Bi₂Rh₂S₂10,24 has a high temperature structural phase transition, but remains non-superconducting down to 0.5 K, and the neighboring Bi₂Rh₃.₅S₂24 has no structural phase transition, but becomes superconducting at Tc ≈ 1.7 K. The discovery of superconductivity in Bi₂Rh₃.₅S₂ motivated us to extend our exploration for superconducting compounds to the Rh-In-S system, which has not yet been fully investigated with only one compound, Rh₂In₃S₁₀, reported.

In this article, we present details of the crystal growth and characterization of the transition-metal chalcogenide superconductor Rh₃In₄S₄. Measurements of transport properties, magnetization and specific heat confirm bulk superconductivity of Rh₃In₄S₄ at Tc ~ 2.25 K and we report other superconducting properties from the above measurements. The upper critical field, Hc2, shows good agreement with the Helfand-Werthamer (HW) theory. We also present the observation of a peak effect in this material by means of transport measurements.

II. EXPERIMENTAL METHODS

Single crystals of Rh₃In₄S₄ were produced using a solution growth technique22,25,26. A mixture of elemental Rh, In and S was placed in a 2 mL fritted alumina crucible27,28 with a molar ratio of Rh:In:S = 55:22.5:22.5 and sealed in a silica ampoule under a partial pressure of high purity argon gas. The sealed ampoule was heated to 1150°C over 12 hours and held there for 3 hours. After that, it was cooled to 950°C over 50 hours and excess liquid was decanted using a centrifuge. Single crystals of Rh₃In₄S₄ grew as tetragonal rods with typical size of ~ 0.5 × 0.5 × 2 mm³ as shown in the inset of Fig. 2(b).

Single crystal X-ray diffraction data were collected using a Bruker SMART APEX II CCD area-detector diffractometer29 equipped with Mo Kα (λ = 0.71073Å) radiation. Integration of intensity data was performed by the SAINT-Plus program, absorption corrections30 by SADABS, and least-squares refinements by SHELXL31, all in the SMART software package. Lattice parameters were refined using single crystal diffraction data and are summarized in Table I. Atomic coordinates and displacement parameters with full site occupancy for Rh₃In₄S₄ are derived from the single crystal diffraction and given in Table II. Powder X-ray diffraction data were collected using a Rigaku Miniflex II diffractometer at room temperature (Cu Kα radiation). Samples for powder X-ray diffraction was prepared by grinding single crystals and spreading them onto a thin grease layer coated single crystal Si, zero background puck. Powder X-ray diffraction data were analyzed using the GSAS32,33 program.

| Formula | Rh₃In₄S₄ (293 K) |
|---------|----------------|
| Formula weight | 1485.89 |
| Z-formula units | 2 |
| Space group | 14/m m m (139) |
| a (Å) | 7.7953(3) |
| c (Å) | 8.8583(3) |
| Volume (Å³) | 538.25(5) |
| Density (g/cm³) | 9.339 |

The ac resistivity (f = 17 Hz) was measured as a function of temperature and field by the standard four probe method in a Quantum Design (QD), Physical Property
TABLE II. Atomic coordinates and equivalent isotropic displacement parameters of Rh$_9$In$_4$S$_4$ at 293 K.

| Atom | Wyck  | Symm. | x   | y   | z   | $U_{eq}$ ($\AA^2$) |
|------|-------|-------|-----|-----|-----|---------------------|
| In1  | 4e    | 4mm   | 0   | 0   | 0.1872(3) | 0.027(1) |
| In2  | 4d    | -4m2  | 0.5 | 0   | 0.25  | 0.019(1) |
| Rh1  | 8f    | ..2/m | 0.25| 0.25| 0.25  | 0.067(1) |
| Rh2  | 8i    | m2m   | 0.3011(3)| 0   | 0    | 0.019(1) |
| Rh3  | 2b    | 4/mmm | 0   | 0   | 0.5   | 0.012(1) |
| S    | 8h    | m.2m  | 0.2079(7)| 0.2079(7)| 0.5   | 0.038(2) |

Measurement System (PPMS) instrument. Four Pt wires with diameters of 25 $\mu$m were attached to the samples using EpoTek-H20E silver epoxy or DuPont 4929N silver paint. The contact resistance was $\sim 0.5\Omega$. The specific heat was measured by using the relaxation method in the PPMS. The $^3$He option was used to obtain measurements down to 0.4 K. The total uncertainty of the specific heat data is $\sim 5\%$. The DC magnetization measurements were performed in a QD, Magnetic Property Measurement System (MPMS).

III. RESULTS

A. Structure

![Figure 1](image1.png)

**Figure 1.** (a) Unit cell of Rh$_9$In$_4$S$_4$, with Rh1-centered octahedra shaded in blue. Rh1 and S atoms are shown as ellipsoids with 90% probability. (b)-(d) show the detailed configurations of Rh1-, Rh2-, and Rh3-centered octahedra, together with representative bond distances. Numbers overlaid with colored spheres denoted atoms listed in Table.II.

**Figure 2.** (a) Reciprocal lattice viewed along (001) zone for Rh$_9$In$_4$S$_4$. Green dots denote a 2 x 2 main lattice reflections of the average structure given in Table.1; four-fold, more diffuse, clusters around the green dots denote weak reflections of modulated lattice, with a modulation vector of [0.17 0.17 0] (red arrow). (b) Powder diffraction pattern of Rh$_9$In$_4$S$_4$. The red line represents the calculated diffraction pattern based on lattice parameters obtained from the single crystal diffraction analysis. The blue line represents the difference between the experimental and calculated intensities. The inset shows a photo of single-crystalline Rh$_9$In$_4$S$_4$ on a millimeter grid and the arrow indicates the [1 0 0] direction.

in the tetragonal symmetry I4/mmm ($a = 7.7953(3)\ \text{Å}$, $c = 8.8583(3)\ \text{Å}$). Powder pattern was fitted with LeBail refinement and obtained $R_p = 7.3\%$ as shown in Fig. 2(b). Lattice parameters obtained from this measurement are in good agreement (less than 0.2%) with single crystals data.

The composition was refined as Rh$_9$In$_4$S$_4$, consistent with Rh$_{2.2(1)}$InS measured by electron probe microanalyzer (EPMA). The lattice parameters and atomic coordinates are listed in Table. I and Table. II, respectively. As in the case of Bi$_2$Rh$_2$S$_2$, all Rh atoms in Rh$_9$In$_4$S$_4$ are six-coordinated forming slightly distorted octahedra. Of these, Rh1 and Rh2 are surrounded by 4 In and 2 S atoms, whereas Rh3 by 2 In and 4 S atoms, see Fig. 1(b)-(d). Whereas Rh2 and Rh3 octahedra sit on edges or face centers of the unit cell, Rh1 octahedra are located at (1/4...
1/4 1/4) and equivalent sites. The arrangement of these Rh1-centered octahedra is similar to those in Perovskites, except that they share edges (In1-In2) in the ab plane and vertices along c, whereas in Perovskites only corners are shared. Apparently, the pivot-and-rock motion of these Rh1-centered octahedra is restricted in ab plane, resulting in ellipsoid elongation for the Rh1 and S atoms, Fig. 1(a). Viewing along the c axis, Rh1 and S atoms form a zig-zag chains extending along c, and their disorder can easily lead to structure modulation, as observed in many other structures, e.g., Sc$_4$Mg$_2$Cu$_{115-\delta}$Ga$_{7.5}$.

Indeed, careful examination of reciprocal space from single crystal intensity data confirms that the structure is a modulated structure. With a cut-off intensity of 3σ, we were able to identify a modulation vector of [0.17 0.17 0], see Fig. 2(a). However, due to the weakness of the modulation reflections, no model of any modulated structured has been acceptable (so far). Since the results of an average structure refinement are sufficient for our current discussions, herein we will no longer focus on the detailed modulated structure, but rather the averaged structure.

### B. Physical properties of Rh$_9$In$_4$S$_4$

Figure 3 shows the temperature dependent resistivity of Rh$_9$In$_4$S$_4$ for current flowing along the [1 0 0] direction. The resistivity decreases monotonically with decreasing temperature, showing metallic behavior and a clear sharp transition to zero resistivity below $T_c = 2.25$ K, indicating a superconducting transition of this material (Fig. 3(a)). The residual resistivity ratio (RRR) ($\rho_{300 K}/\rho_{5.5 K}$) is 1.2. Figure 3(b) show the zero-field-cooled (ZFC) and field-cooled (FC) magnetization data of Rh$_9$In$_4$S$_4$ and clearly indicates over 95% shielding fraction at 1.8 K. Also in the experimental data we can see a weak negative curvature in resistivity at higher temperatures as shown in Fig. 3(c).

Figure 4 shows the low temperature specific heat data of Rh$_9$In$_4$S$_4$. A fit for $C_p/T = \gamma + \beta T$ from 2.3 to 3.5 K for the normal state, as shown in the inset of Fig. 4, yielded the Sommerfeld coefficient, $\gamma = 34 \text{ mJ mol}^{-1} \text{K}^{-2}$ (or $\sim 2 \text{ mJ mol-atomic}^{-1} \text{K}^{-2}$), $\beta = 3.22 \text{ mJ mol}^{-1} \text{K}^{-4}$. From the $\beta$ value we estimate the Debye temperature, $\Theta_D = 217$ K, using the relation $\Theta_D = (12\pi^2 n R / (5 \beta))^{1/3}$, where $n$ is the number of atoms per formula unit and $R$ is the universal gas constant.

With a large superconducting volume fraction, the specific heat data are expected to reveal a clear anomaly at $T_c$. We obtained the $T_c = 2.22$ K and the specific heat jump of $\Delta C = 125 \text{ mJ mol}^{-1} \text{K}^{-1}$ by using an equal entropy construction to the low temperature specific heat data. Given that $T_c = 2.25$ K from the resistivity, $T_c \approx 2.24$ K from the magnetization and $T_c \approx 2.22$ K from the specific heat, we can state $T_c \sim 2.25$ K for Rh$_9$In$_4$S$_4$.

$\Delta C/\gamma T_c = 1.66$ is an important measure of electron-phonon coupling strength, which is stronger here, than the BCS weak-coupling limit of 1.43. The red colored line if Fig. 4 represents the BCS calculation for the weak limit.

The electron-phonon coupling constant $\lambda_{e-ph}$ can be estimated from the McMillan equation [27] for the superconducting transition temperature, for phonon mediated superconductors,

$$T_c = \frac{\Theta_D}{1.45} \exp \left[ - \frac{1.04(1 + \lambda_{e-ph})}{\lambda_{e-ph} - \mu^* (1 + 0.62\lambda_{e-ph})} \right]$$  \hspace{1cm} (1)
where \( \mu^* \), the Coulomb pseudopotential, has a value often between 0.1 and 0.2 and usually is taken as 0.13. Similar values of \( \mu^* \) have been used in other Rh-containing chalcogenides. Using \( \Theta_D = 217 \text{ K} \) and \( T_c = 2.22 \text{ K} \) we estimated \( \lambda_{c-ph} = 0.56 \). A difference of \( \mu \) from the assumed value of 0.13 will give a different value of \( \lambda_{c-ph} \). For example, \( \lambda_{c-ph} = 0.5 \) if \( \mu = 0.1 \) and \( \lambda_{c-ph} = 0.71 \) if \( \mu = 0.2 \). The value of \( \lambda_{c-ph} \) indicates the sample is an intermediate coupled superconductor. The ratio between BCS-coherence length and mean free path can be written as \( \xi_{BCS}/l = (0.18h\mu_0e^2)/(k_B T_\text{c} \mu^* \cdot \mu_0) \). Using the values of \( \rho_0 = 180 \mu\Omega \text{ cm} \), \( T_c = 2.24 \text{ K} \), \( m^* = m_e(1 + \lambda_{c-ph}) \) and assuming electron density for typical metal, \( n \approx 10^{27} - 10^{28} \text{ m}^{-3} \), we can calculate \( \xi_{BCS}/l \approx 20-200 \). This value is much greater than one, indicating that RhIn\textsubscript{4}S\textsubscript{4} is unambiguously in the dirty limit.

FIG. 5. Low temperature resistivity as a function of (a) temperature and (b) field for several applied currents for \( H \parallel \langle 0 \ 1 \ 1 \rangle \) configuration where current flow along the \[1 \ 0 \ 0\] direction.

In some type-II superconductors, a sharp maximum in the temperature or field dependence of critical current observed below \( H_{c2}(T) \) is called the “peak effect”\textsuperscript{39-43}. Several mechanisms have been proposed for the explanation of the peak effect such as matching mechanism\textsuperscript{44}, elementary pinning by weakly superconducting regions\textsuperscript{45,46}, reduction in elastic moduli of the flux line lattice and the synchronization of the flux line lattice\textsuperscript{47,48}. However, the underlying physics is not yet fully understood so far. Figure 5(a) shows the temperature dependence of resistivity data for several applied fields and measuring currents for an \( H \parallel \langle 0 \ 1 \ 1 \rangle \) configuration. For \( I = 0.1 \text{ mA} \), at field of \( \sim 0.2 \text{ T} \) the transition is quite sharp. However for moderate fields, such as 0.8 or 1.2 T, the resistivity data show a kink in between onset and offset of the transition and, for further increase of the field (e.g. 1.8 T), the resistivity drops to zero before increasing to a finite value. For higher currents these anomalies in resistivity become more prominent and at higher fields, resistivity just show a dip before increasing and then gradually going to zero. The anomalies in the resistance are seen more clearly in the resistivity vs. magnetic field at fixed temperatures for the different values of measuring current (\( H \parallel \langle 0 \ 1 \ 1 \rangle \) configuration) as shown in Fig. 5(b). With the increase of field, the resistivity is essentially zero up to a critical field (\( H^* \)) and it starts to increase. For further increase of field, the resistiv-

FIG. 6. Upper critical field \( H_{c2} \) vs \( T \) of RhIn\textsubscript{4}S\textsubscript{4} for (a) \( H \parallel I \) and (b) \( H \perp I \) configurations with current along \( a \)-axis. Lower and upper insets show the criteria which was used to obtained the data points. Solid and open symbols represent the data obtained by field scans and temperature scans respectively. The blue solid line in (a) indicates the HW calculations for the dirty limit. In (b), lower and upper insets show the resistivity anomalies due to the peak effect and \( H^* \) and \( T^* \) data represent by solid and open black squares.
ity reaches maximum and goes to zero again before increasing to the normal state. For larger current, $H^*$ decreases and height of the peak increases. It should be emphasized that there were no anomalies in the transition observed when the current is parallel to the magnetic field. Similar peak effect data has been observed in several compounds including Nb$_4^{49}$, CeRu$_2^{50-52}$, NbSe$_2^{53}$, V$_3$Si$_{14}$, ReCr$_5^{55}$, Yb$_2$Rh$_4$Si$_{13}^{56,57}$, and MgB$_2^{58-60}$. However we observed this effect at low current densities, $j$, between 0.3-3 A cm$^{-2}$ in contrast with other superconducting materials ($j \gg 10$ A cm$^{-2}$)$^{55-58,59,60}$. The $H-T$ phase diagrams obtained from the low temperature $R$ vs. $T$ and $R$ vs. $H$ measurements are presented in Fig. 6 for $I = 0.3$ mA. Figure 6 (a) and (b) show $H \parallel [0 1 0]$ and $H \parallel [0 0 1]$ configurations and the upper and lower insets of each figure show the criteria used to determine $H_{c2}$ and $T_c$. Open and closed symbols represent data obtained from temperature scans and field scans respectively. As noted above, the peak effect is only detectable in the $H \parallel [0 0 1]$ configuration. Comparison of $H_{c2}$ in $H \parallel [1 0 0]$ and $H \parallel [0 1 1]$ configurations indicates virtually isotropic $H_{c2}$ behavior. For a one band, type II superconductor the orbital upper critical field is given by Helfand-Wethamer theory$^{61}$ and can be estimated from $H_{c2} = -AT_c dH_{c2}/dT$, where $A = 0.73$ for clean limit and 0.69 for the dirty limit. The slope of the curve in the vicinity of $T_c$ (for the offset criteria) is -1.69 T K$^{-1}$. Using this value, the calculated $\mu_0 H_{c2}$ is 2.78 T for the clean limit and 2.62 T for the dirty limit. The blue solid line in Fig. 6 (a) represents the calculated HW curve for the dirty limit (Ref. 61 equation 24), and it shows a good agreement with the experimental data. By using both normal state and superconducting state specific heat data, one can obtain the thermodynamic critical field, $\mu_0 H_c(T)$ as a function of temperature from equation 2

$$\frac{\mu_0 V_m H_c(T)^2}{2} = \int_{T_c}^{T} \Delta S(T')dT$$

in which $\Delta S(T)$ is the entropy difference between the normal and superconducting states and $V_m$ (16.2$\times$10$^{-5}$ m$^3$ mol$^{-1}$) is the molar volume. The calculated value of $\mu_0 H_c(T=0)$ is 25 mT for Rh$_9$In$_4$Si$_4$ and it is much smaller than $\mu_0 H_{c2}(0)$=2.62 T as expected for type II superconductor. The value of $\mu_0 H_{c2}(0)$ is well below the Pauli paramagnetic limit$^{52,53}$ of $\mu_0 H_{c2}^p(0)$=1.84 Tc = 4.1 T, suggesting an orbital pair-breaking mechanism. We also can estimate the Ginzburg-Landau(GL) coherence length$^{36}$, $\xi_{GL} \approx 94$ Å by using the relation $\Phi_0 = (2\pi \xi_{GL}^2 T_c)$, in which $\Phi_0$ is the quantum flux and estimated $\mu_0 H_{c2}(T_c)$=$\Phi_0/(2\pi \xi_{GL}^2 T_c)$, in which $\Phi_0$ is the quantum flux and estimated $d(\mu_0 H_{c2}(T_c))/dT$ to be -1.69 T K$^{-1}$ near $T_c$. London penetration depth for the dirty limit can be written as$^{62}$,

$$\lambda^{-2}(T) = \frac{4\pi^2 \Delta(T)}{(c^2 \hbar \rho_{0,cgs}) tanh(\Delta(T)/(2T))}$$

where $\Delta(T)$ is temperature dependence of the superconducting gap energy and all parameters are in cg units. Near $T_c$,

$$\Delta^2(T \to T_c) = \frac{8\pi^2 T^2 \xi(3)}{\zeta(3)} (1 - \frac{T}{T_c})$$

$$\lambda^{-2}(T \to T_c) = \frac{4\pi^2}{c^2 \hbar \rho_{0,cgs}} \frac{\Delta^2(T \to T_c)}{2T_c \kappa B}$$

$$\lambda^2(T \to T_c) = \frac{\lambda^2_{GL}}{(1 - \frac{T}{T_c})^2}$$

(4)

where $\zeta$ is the Riemann zeta function and $\zeta(3) \approx 1.202$. The expression in Eq. 4 can be reduced and converted to SI units as $\lambda(T \to T_c) = 0.00064(\rho_0/(T_c(1 - T/T_c)) = \lambda_{GL}/\sqrt{(1 - T/T_c)}$, where $\rho_0$ is in SI units. Using $\rho_0 = 180 \times 10^{-8}$ $\Omega$ m and $T_c = 2.25$ K, we can obtain $\lambda_{GL} = 0.00064(\rho_0/T_c \approx 5750$ Å. Based on $\xi_{GL}$ and $\lambda_{GL}$ values, estimated GL parameter $\kappa = \lambda_{GL}/\xi_{GL}$ is ~61. Jump of the specific heat and slope of $H_{c2}$ at $T_c$ can be calculated from the Rutger’s relation$^{65,66}$

$$\Delta C/T_c = (1/8\pi\kappa^2)(dH_{c2}/dT)^2 [T_c]$$

(5)

where $\Delta C$ in units of erg cm$^{-3}$ K$^{-1}$ and slope $H_{c2}$ in units of Oe K$^{-1}$. Using the molar volume, $V_m = 162.1$ cm$^3$ mol$^{-1}$ we obtain the converted $\Delta C = 7710$ erg cm$^{-3}$ K$^{-1}$. From the value of $H_{c2}$ slope near $T_c$, $dH_{c2}/dT = 16900$ Oe K$^{-1}$, we obtained a similarly large $\kappa$ value of 57. This considerably large $\kappa$ value indicates that Rh$_9$In$_4$Si$_4$ is an extreme type II superconductor. A summary of the measured and derived superconducting state parameters for Rh$_9$In$_4$Si$_4$ is given in Table III.

| Rh$_9$In$_4$Si$_4$ property | Value |
|-----------------------------|-------|
| $T_c$ (K)                   | 2.25(2) |
| $\gamma$ (mJ mol$^{-1}$ K$^{-2}$) | 34.0(4) |
| $\beta$ (mJ mol$^{-1}$ K$^{-4}$) | 3.22(5) |
| $\Theta_D$ (K)              | 217 |
| $\Delta C$ (mJ mol$^{-1}$ K$^{-1}$) | 125(4) |
| $\Delta C/\gamma T_c$       | 1.66(6) |
| $\lambda_{c-\phi h}$        | 0.56 |
| $\rho_0$ (\mu$\Omega$ cm)  | 180 |
| $H_{c2}(T = 0)$ (T) (clean limit) | 2.78 |
| $H_{c2}(T = 0)$ (T) (dirty limit) | 2.62 |
| $H_{c2}^{q}(T = 0)$ (T)      | 4.1 |
| $H_{c2}(T = 0)$ (mT)         | 25 |
| $\xi_{BCS}/l$               | 20-200 |
| $\xi_{GL}$ (Å)              | 94 |
| $\lambda_{GL}$ (Å)          | 5750 |
| $\kappa = \lambda_{GL}/\xi_{GL}$ | 61 |
| $\kappa$ (from Rutger’s relation) | 57 |
IV. CONCLUSIONS

We report the synthesis, crystal structure and characterization (such as resistivity, magnetization and specific heat) of superconducting Rho3In4Sn with a bulk superconducting transition of $T_c \sim 2.25$ K and large value of GL parameter $\kappa \sim 60$. Rho3In4Sn is found to be a type II and intermediate-coupling superconductor. The calculated values for the Sommerfeld coefficient and the Debye temperature are 34 mJ mol$^{-1}$ K$^{-2}$ and 217 K respectively. The temperature dependence of the specific heat shows a larger jump $\Delta C/\gamma \sim 1.66$ at $T_c$, than the BCS weak coupling limit. The upper field critical shows a good agreement with the HW theory. We have shown a direct evidence of a peak effect from resistivity in Rho3In4Sn single crystals as a function of both temperature and magnetic field. Further studies of superconducting properties and peak effect of this material will be useful to understand the nature of their mixed state and pinning properties.

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