Dust Rotational Dynamics in C-shocks: Rotational Disruption of Nanoparticles by Stochastic Mechanical Torques and Spinning Dust Emission

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Abstract

Polycyclic aromatic hydrocarbons (PAHs) and nanoparticles are expected to play an important role in many astrophysical processes due to their dominant surface area, including gas heating, chemistry, star formation, and anomalous microwave emission. In dense magnetized molecular clouds where C-shocks are present, PAHs and nanoparticles are widely believed to originate from grain shattering due to grain–grain collisions. The remaining question is whether these nanoparticles can survive in the dense and hot shocked regions, and how to constrain their size and abundance with observations. In this paper, we present a new mechanism to destroy nanoparticles in C-shocks based on centrifugal stress within rapidly spinning nanoparticles spun up by stochastic atomic bombardment, which is termed rotational disruption. We find that, due to supersonic neutral gas-charged grain drift in C-shocks, nanoparticles can be spun up to suprathermal rotation by stochastic torques exerted by supersonic neutral flow. The resulting centrifugal stress within suprathermally rotating nanoparticles can exceed the maximum tensile strength of grain material ($S_{\text{max}}$), resulting in rapid disruption of nanoparticles smaller than $a \sim 1$ nm for $S_{\text{max}} \sim 10^8$ erg cm$^{-3}$. The proposed disruption mechanism is shown to be more efficient than thermal sputtering in controlling the lower cutoff of grain size distribution in C-shocks. We model microwave emission from spinning nanoparticles in C-shocks subject to supersonic neutral drift and rotational disruption. We find that suprathermally rotating nanoparticles can emit strong microwave radiation, and both peak flux and peak frequency increase with increasing shock velocity. We suggest spinning dust as a new method to constrain nanoparticles and trace shock velocities in shocked dense regions.

Key words: dust, extinction – radiation mechanisms: non-thermal

1. Introduction

Polycyclic aromatic hydrocarbons (PAHs) and very small dust grains (hereafter referred to as nanoparticles) are expected to play an important role in gas heating via photoelectric effect (Weingartner & Draine 2001) and chemistry because they contribute the dominant surface area of dust grains (see Akimkin et al. 2013). In dense, low-ionization molecular clouds, nanoparticles are believed to affect cloud dynamics and star formation processes such as ambipolar diffusion (Mestel & Spitzer 1956) owing to their dominant charge carrier (see Zhao et al. 2016 and references therein).

Nanoparticles are expected to be depleted in dense regions owing to grain coagulation and accretion of atoms on the grain surface (Draine 2003; Tibbs et al. 2016). At the same time, grain–grain collisions due to grain acceleration by magnetohydrodynamic turbulence (Yan & Lazarian 2003; Hoang et al. 2012) can shatter large grains ($a \gtrsim 0.1$ $\mu$m) to form nanoparticles. In a strong radiation field such as massive stars and supernovae, nanoparticles can be produced by rotational disruption of large grains by radiative torques (Hoang et al. 2019). When a shock is passing through a dense cloud, nanoparticles can also be formed by grain–grain collisions (Jones et al. 1994; Tielens et al. 1994).

Interstellar shocks are ubiquitous in the interstellar medium (ISM). In magnetized dense clouds with a low ionization fraction, neutral gas and neutral grains can drift relative to charged grains/ions that are coupled to the magnetic field. When the shock speed is lower than the magnetosonic speed, physical parameters are continuous throughout the shock, for which the term C-type shocks is introduced (Draine 1980; see also Ciolek et al. 2004). As a result, collisions between neutral small grains and charged large grains can shatter the grains and form nanoparticles, including PAHs, nanosilicates, and nanodiamonds (Jones et al. 1996; Guillet et al. 2011). The remaining question is (i) whether nanoparticles can survive passing the C-shock and (ii) how to constrain the size and abundance of this nanodust population in shocked regions.

The first issue is important for understanding the composition of interstellar nanoparticles, which can help to shed light on the exact carrier of anomalous microwave emission (Hoang et al. 2016; see Dickinson et al. 2018 for a review). The second issue is important for a quantitative understanding of the effect of nanoparticles on the cloud dynamics and chemistry in interstellar shocks.

Due to the lack of UV/optical photons to trigger mid-IR emission, the potential new technique to probe PAHs and nanoparticles in shocked dense regions is to use microwave emission produced by rapidly spinning nanoparticles (Draine & Lazarian 1998; Hoang et al. 2010, 2016, 2018b). Spinning dust emissivity depends mostly on the rotation of nanoparticles, grain dipole moment, and its abundance and size distribution.
in which the smallest nanoparticles are the most important emitters (Hoang et al. 2011).

Rotational dynamics of interstellar dust grains is a fundamental astrophysical problem. The grain rotation controls a variety of astrophysical observations, in both emission and polarization. For instance, the rapid rotation of nanoparticles can emit electric dipole radiation, which is an important galactic foreground contaminant to cosmic microwave background (CMB) radiation. In particular, suprathermal rotation can help dust grains to be efficiently aligned with magnetic fields (Hoang & Lazarian 2016a; see Andersson et al. 2015 and Lazarian et al. 2015 for recent reviews). Dust polarization induced by aligned grains is a powerful tracer of cosmic magnetic fields and also a major foreground of CMB polarization. In particular, rotational disruption due to centrifugal stress within extremely fast rotating grains spun up by radiative torques can control the maximum cutoff of grain size distribution (Hoang et al. 2019). Rotational dynamics of nanoparticles and dust grains has been well studied for the homogeneous diffuse ISM, molecular clouds (Draine & Lazarian 1998; Hoang et al. 2010), and turbulent media (Hoang et al. 2011). Yet a detailed study of grain rotation in interstellar shocks is not yet available.

The size distribution of PAHs and nanoparticles in the shocked dense regions is poorly known owing to the lack of observational constraints. In the diffuse ISM, the smallest size of nanoparticles of \( a \sim 0.35 \text{ nm} \) is determined by thermal sublimation (Guhathakurta & Draine 1989; Hensley & Draine 2017). In very hot plasma, thermal sputtering takes over (Draine & Salpeter 1979). In dense cold clouds, due to the lack of UV photons, both sublimation and thermal sputtering are not effective, such that one can expect a much smaller lower cutoff of the grain size distribution. In studies of grain shattering, the smallest size of nanoparticles is usually fixed to \( a_{\text{min}} = 0.5 \text{ nm} \) without physical justification (Jones et al. 1996; Guillet et al. 2011). Micelotta et al. (2010) studied the destruction of PAHs in shocks and found that PAHs can be efficiently destroyed by shocks of velocities \( v_s > 100 \text{ km s}^{-1} \). For lower shock velocities, PAHs and smallest nanoparticles (i.e., nanoparticles smaller than several nanometers) are expected to survive the shock passage. As a result, constraining the lower size cutoff and abundance of nanoparticles is of great importance.

In the diffuse ISM, nanoparticles are known to rotate subthermally (i.e., rotational temperature lower than gas temperature) owing to the dominance of rotational damping by electric dipole emission over gas collisional damping (Draine & Lazarian 1998; Hoang et al. 2010; Hoang & Lazarian 2016b). The situation is dramatically different in dense regions where the gas collisional damping becomes dominant over electric dipole emission damping such that nanoparticles can achieve thermal rotation (Hoang et al. 2018b; see Section 4). In C-shocks, where the gas can be heated to high temperatures of \( T_{\text{gas}} \sim 3 \times 10^3 \text{ K} \) (see Section 2), nanoparticles at thermal equilibrium would rotate extremely fast, at frequencies

\[
\frac{\omega_{\text{rot}}}{2\pi} \approx 2.5 \times 10^{10} \left( \frac{T_{\text{gas}}}{3000 \text{ K}} \right)^{1/2} a_{\gamma}^{-5/2} \text{ Hz},
\]

(1)

where \( a \) is the radius of spherical nanoparticles and \( a_{\gamma} = a/(10^{-7} \text{ cm}) \) (see Equation (42)). Therefore, nanoparticles of \( a \lesssim 0.5 \text{ nm} \) can spin at \( \omega_{\text{rot}}/2\pi \gtrsim 1.4 \times 10^{11} \text{ Hz} \), just a factor of 2.6 lower than the critical limit for disruption of \( \omega_{\text{cri}}/2\pi \approx 3.7 \times 10^{11}(0.5 \text{ nm}/a)(S_{\text{max}}/10^{10} \text{ erg cm}^{-3})^{1/2} \text{ Hz} \) (see Equation (43)). As we will see in Sections 3 and 4, supersonic neutral drift can further spin up charged nanoparticles to suprathermal rotation of \( \omega > \omega_{\text{cri}} \), resulting in an instantaneous disruption of the nanoparticle into tiny fragments. This important effect will be quantified in the present paper.

A high fraction of nanoparticles resulting from grain shattering and suprathermal rotation excited by neutral drift are expected to induce strong spinning dust emission at microwave frequencies. On the other hand, rotational disruption can decrease the abundance of smallest nanoparticles, which can decrease the resulting spinning dust emissivity. We will perform a detailed modeling of spinning dust emission in C-shocks, accounting for this destruction effect.

The structure of the present paper is as follows. In Section 2, we describe the C-type shock model in dense magnetized molecular clouds and compute the gas temperature and velocities of neutral, ion, and charged nanoparticles. In Section 3 we will study rotation dynamics of nanoparticles in C-shocks where the supersonic drift of neutrals relative to charged grains is important. We will introduce the rotational disruption mechanism and calculate the minimum size of nanoparticles that can survive the shock passage in Section 4. In Section 5 we calculate spinning dust emissivity from nanoparticles in shocked regions. We will discuss the importance of rotational disruption and potential application of spinning dust for constraining abundance of nanoparticles and shock velocity in Section 6. A short summary of our main results is presented in Section 7.

2. Structures of C-shocks and Grain Drift Velocities

2.1. Shock Structure and Physical Parameters

Let us briefly describe the C-type shock in dense magnetized molecular clouds. In the shock reference frame, the ambient preshock gas flows into the shock such that their physical parameters change smoothly with the distance in the shock. At the shock interface, the neutral and ion velocities are the same as the shock velocity considered in the shock reference frame. Due to the deceleration when colliding with the shock matter, neutrals and ions are slowed down until they move together with the shock front, i.e., \( v_n = v_i = 0 \). Due to magnetic forces, ions and charged grains are coupled to the ambient magnetic field and move slower than neutrals, resulting in \( v_m > v_i \) or drift of neutral gas with respect to charged grains and ions.

We calculate the ion and neutral velocities for the different shock velocities using the one-dimensional plane-parallel Paris-Durham shock model (Flower & Pineau des Forêts 2015). Our initial elemental abundances in the gas, grain cores, ice mantle, and PAHs are the same as in the previous studies (Flower & Pineau des Forêts 2003; Lesaffre et al. 2013; Tram et al. 2018).

Different types of shocks depend on the value of the shock’s entrance speed relative to the entrance magnetosonic speed \( v_m \), which is defined in charged fluid as

\[
v_m = \left( \frac{\epsilon^2 + \frac{B^2}{4\pi M^2}}{\rho_c} \right)^{1/2},
\]

(2)

where \( \rho_c \) is the total mass density of charged particles, including ions and charged dust grains (e.g., PAHs,
nanosilicates, and large grains), and \( c_s \) and \( B/\sqrt{4\pi\rho_c} \) are the sound speed and Alfvén speed of the charged fluid, respectively. The C-shock term is accordingly given when the shock speed is lower than \( v_m \).

In the case of low ionization (low density of charged particles), Equation (2) yields

\[
v_m \simeq \frac{B}{\sqrt{4\pi\rho_c}} = b v_{m1}, \tag{3}
\]

where \( b \) is a dimensionless magnetization parameter and \( v_{m1} \) is the magnetosonic speed for \( b = 1 \). In our calculations, we find \( v_{m1} = 19.2 \, \text{km s}^{-1} \) or \( v_{m1} = 19.5 \, \text{km s}^{-1} \) for gas density of \( n_H = 10^4 \, \text{cm}^{-3} \) or \( n_H = 10^5 \, \text{cm}^{-3} \), respectively. From Equation (3) one can obtain the scaling between the magnetic field strength and the gas density:

\[
B(\mu G) = b \left( \frac{n_H}{1 \, \text{cm}^{-3}} \right)^{1/2}, \tag{4}
\]

where we have assumed homogeneous ionization. For the standard ISM, one has \( b \sim 1 \), and \( b \sim 1–2 \) for dense regions driven by outflows (see, e.g., Gusdorf et al. 2015). In this paper, we adopt \( b = 2 \), which enables us to explore a wide range of C-shock velocity.

Table 1 presents the main physical parameters, including proton number density \( n_H \), gas temperature \( T_{\text{gas}} \), hydrogen ionization fraction \( x_H \), heavy-element ionization fraction \( x_M \), radiation strength relative to the average interstellar radiation field (ISRF; Mathis et al. 1983) \( \chi \), dust grain temperature \( T_d \), molecular hydrogen fraction \( y \), and fraction of PAHs in the shock \( x_{\text{PAH}} \).

| Parameters          | Model A | Model B | Model C |
|---------------------|---------|---------|---------|
| \( v_m \) (km s\(^{-1}\)) | 5–30    | 5–30    | 5–30    |
| \( n_H \) (cm\(^{-3}\))    | 10\(^5\) | 10\(^6\) | 10\(^6\) |
| \( T_{\text{gas}} \) (K)   | 10      | 10      | 10      |
| \( T_d \) (K)            | 10      | 10      | 10      |
| \( \chi \)            | 0.01    | 0.01    | 0.01    |
| \( x_H \equiv n(H^+)/n_H \) | 10\(^{-6}\) | 10\(^{-6}\) | 10\(^{-6}\) |
| \( x_M \equiv n(M^+)/n_H \) | 10\(^{-6}\) | 10\(^{-6}\) | 10\(^{-6}\) |
| \( x_{\text{PAH}} \equiv n(\text{PAH})/n_H \) | 10\(^{-6}\) | 10\(^{-6}\) | 10\(^{-6}\) |
| \( y = 2n(H_2)/n_H \)   | 0.999   | 0.999   | 0.999   |
| \( B(\mu G) = b_nH^{1/2} \) | 200     | 632     | 2000    |

Note.

\(^{a}\) Here \( b = 2 \) is assumed.

is a much more gradual process and spreads over a much larger volume. For instance, the length \( L \) of the C-type shock can be up to \( 3 \times 10^{16} \, \text{cm} \), or \(<0.01 \, \text{pc} \) with preshock density \( n_H = 10^4 \, \text{cm}^{-3} \). In a denser cloud (bottom panel), however, the gas is swept and compressed by shock much stronger and earlier. This therefore makes the gas hotter, and the gas temperature increases much earlier compared to a less dense cloud. Radiative cooling also occurs faster, narrowing the shocked region to \( L \sim 10^{15} \, \text{cm} \) (see bottom panel).

### 2.2. Drift Velocities

Figure 2 shows the velocity structure of neutrals (\( v_n \)) and ions (\( v_i \)), as well as the drift velocity of neutrals relative to ions (\( v_{\text{drift}} = v_n - v_i \)), assuming \( n_H = 10^4 \, \text{cm}^{-3} \). The dimensionless drift parameter is defined as \( \sigma_d = v_{\text{drift}}/v_{\text{th}} \), where \( v_{\text{th}} = (2kT_{\text{gas}}/m_H)^{1/2} \) is the thermal gas velocity.

The drift velocity \( v_{\text{drift}} \) rises and reaches the maximum value at the middle of the shock and then declines to zero. The drift parameter, \( \sigma_d \), increases rapidly with \( z \) and then declines when the gas is heated to high temperatures. Note that the peak of \( \sigma_d \) does not coincide with the peak of \( v_{\text{drift}} \) owing to the effect of \( v_{\text{th}} \) or \( T_{\text{gas}} \).

Figure 3 shows the results for \( n_H = 10^6 \, \text{cm}^{-3} \). Compared to Figure 2 (\( n_H = 10^4 \, \text{cm}^{-3} \)), gas temperatures are much higher...
as a result of collisional heating. The shock length is also narrower owing to faster radiative cooling.

3. Rotational Dynamics of Dust Grains in C-type Shocks

3.1. Collisions with Purely Atomic Gas

In dense, low-ionization regions, collisions with gas atoms and molecules play an important role in grain rotational dynamics. We first consider rotational damping and excitation induced by collisions of purely hydrogen thermal gas with a spherical grain. This situation is the same as those derived in Jones & Spitzer (1967), but here we describe in more detail for convenience. The treatment below is also valid for molecular gas with $n_H = 2n(H_2)$.

The well-known damping process for a rotating grain is sticking collision with gas atoms, followed by thermal evaporation. Let us consider a grain rotating along the $z$-axis with angular velocity $\omega_z$. The angular momentum carried away

![Figure 2](image1.png)

![Figure 3](image2.png)

Figure 2. Velocity profiles of neutral ($v_n$), ion and charged grains ($v_i$), and their relative velocity ($v_{drift}$) in the C-shocks with the same parameters as in Figure 1. The dashed line shows the drift parameter $s_d = v_{drift}/v_{th}$, which is dimensionless. The drift velocity increases with the shock velocity, but $s_d$ is slightly changed owing to an increased thermal velocity.

Figure 3. Same as Figure 2, but with $n_H = 10^6$ cm$^{-3}$. Higher thermal and drift velocities but slightly lower values of $s_d$ (dimensionless drift parameter) are observed.
by an H atom from the grain surface is given by
\[ \delta l_z = I_m \omega_z = m_H r^2 \omega_z = m_H a^2 \sin^2 \theta \omega_z, \]
where \( r \) is the distance from the atom to the spinning axis \( z \), \( I_m = m_H r^2 \) is the inertial moment of the hydrogen atom of mass \( m_H \), \( \theta \) is the angle between the \( z \)-axis and the radius vector, and \( r = a \sin \theta \) is the projected distance to the center. In an interval of time, there are many atoms leaving the grain surface from the different location, \( \theta \). Then, assuming the isotropic distribution of \( \theta \) for the atoms leaving the grain, we can evaluate the mean angular momentum carried away per H atom. Thus, we can replace \( \sin^2 \theta = \langle \sin^2 \theta \rangle = 2/3 \), which gives rise to
\[ \langle \delta l_z \rangle = \frac{2}{3} m_H a^2 \omega_z. \] (6)

Using the collision rate of atomic gas, \( R_{\text{coll}} = n_H \nu a^2 \), one can derive the mean decrease of grain angular momentum per unit time of:
\[ \langle \Delta l_z \rangle = \frac{\langle \delta l_z \rangle}{\Delta t} = -R_{\text{coll}} \langle \delta l_z \rangle = -\frac{2}{3} m_H n_H \pi a^4 \omega_z \langle \nu \rangle. \] (7)

The mean velocity is defined by
\[ \langle \nu \rangle = \int v^4 \pi v^2 e^{-m_H v^2/2kT_{\text{gas}}} v^2 \nu \, dv = \left( \frac{8kT_{\text{gas}}}{\pi m_H} \right)^{1/2} , \]
where \( Z = (m_H/2\pi kT_{\text{gas}})^{3/2} \) is the normalization factor of the Boltzmann distribution of gas velocity.

Thus, the gas damping rate is
\[ \langle \Delta l_z \rangle = -\frac{2}{3} m_H n_H \pi a^4 \omega_z \left( \frac{8kT_{\text{gas}}}{\pi m_H} \right)^{1/2} \]
\[ = -\frac{I_{\omega_z}}{\tau_H} , \]
where \( I = 8\pi \rho a^5/15 \) is the inertia moment of a spherical grain, \( \rho \) being the dust mass density, and the characteristic rotational damping time \( \tau_H \) reads
\[ \tau_H = \frac{3 I}{4\sqrt{\pi} m_H n_H \pi a^4} \]
\[ \approx 1.05 \times 10^3 \alpha_{-7} \rho \left( 30 \text{ cm}^{-3} \right) \left( 100 \text{ K} \right)^{1/2} \text{ yr.} \] (11)

Now, let us estimate the rotational excitation of grains due to atomic bombardment.\(^5\) Each atom colliding with the grain surface at radius \( r \) induces an impulsive torque of \( r \times m_H \nu \), such that the increase of \( \langle \delta l_z \rangle^2 \) from each impact becomes
\[ \langle \delta l_z \rangle^2 = (\nu m_H \nu)^2 = m_H a^2 r^2 . \] (12)

When averaging the the grain surface, one has \( \langle \nu^2 \rangle = a^2/2 \), and Equation (12) becomes
\[ \langle \delta l_z \rangle^2 = \frac{1}{2} m_H \nu^2 a^2 . \] (13)

Using the random walk theory for stochastic collisions, one can derive the total increase of \( \langle \delta l_z \rangle^2 \) per unit of time as follows:
\[ \frac{\langle \Delta l_z \rangle^2}{\Delta t} = R_{\text{coll}} \langle \delta l_z \rangle = n_H \nu a^2 m_H \nu^2 a^2/2 . \] (14)

Assuming that thermal evaporation of atoms contributes the same amount of rotational energy as impinging atoms, then, one obtains
\[ \frac{\langle \Delta l_z \rangle^2}{\Delta t} = 2 \frac{\langle \Delta l_z \rangle^2}{\Delta t} = \pi a^2 n_H m_H^2 \nu^3 a^2 , \] (15)
which describes the increase of grain rotational kinetic energy per second.

For thermal gas, the mean rate of energy increase is obtained by integrating Equation (15) over the velocity distribution of gas atoms, which results in
\[ \langle \langle \Delta l_z \rangle^2 \rangle \rangle_H = \left( \frac{\langle \Delta l_z \rangle^2}{\Delta t} \right)_H = \pi a^2 n_H m_H^2 \nu^3 a^2 , \] (16)
where
\[ \langle \nu^3 \rangle = C \int v^3 4\pi v^2 e^{-m_H v^2/2kT_{\text{gas}}} \, dv \]
\[ = 4 \pi^{1/2} \left( 2kT_{\text{gas}} \right)^{3/2} , \] (17)
with \( C = (2\pi kT_{\text{gas}}/m_H)^{3/2} \) being the normalization constant.

Plugging Equation (17) into Equation (16), one obtains the excitation coefficient:
\[ \langle \langle \Delta l_z \rangle^2 \rangle \rangle_H = m_H (8kT_{\text{gas}}/\pi m_H)^{1/2} 4\pi a^4 m_H kT_{\text{gas}} . \] (18)

The one-dimensional excitation coefficient
\[ \langle \langle \Delta l_z \rangle^2 \rangle \rangle_H = 100 \text{ K} \left[ 2m_H (8kT_{\text{gas}}/\pi m_H)^{1/2} a^4 m_H kT_{\text{gas}} \right] \]
\[ = \frac{I_{\omega_T}^2}{\tau_H} , \]
(19)
where \( \omega_T = (2kT_{\text{gas}}/I)^{1/2} \) is the thermal angular velocity.

### 3.2. Ion Collisions, Plasma Drag, and Infrared Emission

Realistic gas consists of atomic and molecular hydrogen, as well as heavier elements. In addition to neutral–grain collisions, nanoparticles are directly bombarded by ions and experience long-distance interaction with passing ions (i.e., plasma drag; Draine & Lazarian 1998; Hoang et al. 2010).

Following Draine & Lazarian (1998), one can define the dimensionless damping \( (F) \) and excitation \( (G) \) coefficients for an interaction process with respect to the damping and excitation coefficients of purely hydrogen neutral–grain collisions. The total damping and excitation rates from various interaction processes are given by
\[ \frac{d(I_{\omega_T})}{dt} = \langle \Delta l_z \rangle_H \times \sum_j F_j , \]
(20)
\[
\frac{d(\omega^2)}{dt} = \frac{\langle (\Delta J_i)^2 \rangle_{\text{H}}}{I} \times G = \frac{3\omega^2}{\tau_{\text{H}}} \times \sum_j G_j,
\]

where \( j = n, i, p, \) and IR denotes neutral–grain, ion–grain, plasma drag, and IR emission, respectively. Note that \( F_j = G_j = 1 \) for grain collisions with purely atomic hydrogen gas.

The diffusion coefficients from ion–grain collisions and plasma drag can be calculated assuming stationary grains, i.e., \( s_d = 0 \), because ions and charged grains are both coupled to the magnetic field.

### 3.3. Rotational Damping and Excitation in C-shocks

We move on to study rotational dynamics of nanoparticles in C-shocks in the presence of supersonic neutral drift relative to charged grains and derive rotational damping and excitation coefficients.

#### 3.3.1. Supersonic Drift

For the supersonic drift of \( s_d \gg 1 \), one can easily obtain the total excitation coefficient as given by Equation (15):

\[
\langle (\Delta J_i)^2 \rangle = n_{\text{H}} m_{\text{H}}^3 v_{\text{drift}} \pi a^4.
\]

From Equations (21) and (22), one obtains the dimensionless excitation coefficient:

\[
G_n(s_d) = \frac{\pi^{1/2} s_d^3}{4}.
\]

#### 3.3.2. Transonic Drift

For the transsonic case (i.e., \( s_d \sim 1 \)), to compute the diffusion coefficients, we follow a similar approach to that in Roberge et al. (1995). Let \( \hat{x} \hat{y} \hat{z} \) be the reference frame fixed to the gas, such that the \( \hat{z} \) axis is directed along the magnetic field and the drift velocity \( v_d \) lies in the \( \hat{y} \hat{z} \) plane with an angle \( \alpha \) with \( \hat{z} \). In this paper, we consider a perpendicular shock such that \( \alpha = 90^\circ \). For the interest of grain rotation, we here consider only spherical grains. Interaction of a supersonic gas flow with nonspherical grains is important for grain alignment (Hoang et al. 2018a) and will be addressed in a future study.

Following Roberge et al. (1995), the dimensionless damping coefficient is given by

\[
\langle \Delta J_i \rangle = -M_0 \langle J_i \rangle \quad \text{for} \quad i = x, y, z,
\]

where \( M_0 \) is a function of drift velocity, and \( M_0 = 1 \) for \( s_d = 0 \), i.e., thermal collision and evaporation.

The diffusion coefficients parallel \((P)\) and transverse \((T)\) to the neutral gas flow are given by (see Equations (3.14)–(3.15) in Roberge et al. 1995)

\[
D_T(s_d) = \frac{3(1 + 2 s_d^2) s_d}{4} M_0(s_d) + (1 - 2 s_d^2) M_2(s_d),
\]

\[
D_P(s_d) = \frac{3}{2} [M_0(s_d) - M_2(s_d)],
\]

where

\[
M_0 = \left( \frac{\sqrt{\pi}}{4} \right) [2(1 + s_d^2) \text{erf}(s_d) - P(3/2, s_d^3)],
\]

\[
M_2 = \left( \frac{\sqrt{\pi}}{4} \right) s_d \text{erf}(s_d) - \left( \frac{3\sqrt{\pi}}{16} \right) s_d^3 P(5/2, s_d^3) + \frac{\sqrt{\pi}}{4} s_d^3 P(3/2, s_d^3),
\]

which are given by Equations (3.9) and (3.16) in Roberge et al. (1995), and \( P \) is the incomplete gamma function.

In the reference frame fixed to the ambient gas, the dimensionless diffusion coefficients become

\[
\langle (\Delta J_i)^2 \rangle = D_T + \frac{T_d}{T_{\text{gas}}},
\]

\[
\langle (\Delta J_z)^2 \rangle = \sin^2 \alpha D_P + \cos^2 \alpha D_T + \frac{T_d}{T_{\text{gas}}},
\]

\[
\langle (\Delta J_y)^2 \rangle = \cos^2 \alpha D_P + \sin^2 \alpha D_T + \frac{T_d}{T_{\text{gas}}},
\]

which results in the dimensionless excitation coefficient

\[
G_n(Z = 0) = \frac{1}{3} \sum_{i=x,y,z} \langle (\Delta J_i)^2 \rangle.
\]

For \( s_d \gg 1 \), \( D_T \) scales as \( s_d^3 \), such that \( G_n \) returns to Equation (23).

#### 3.4. Dynamical Timescales in Shocks

For grain dynamics in shocks, an important dynamical timescale is the flow time of dust grains in the C-shock. The flow time at location \( z \) in the shock can be found by

\[
\tau_{\text{flow}} = \int_0^z \left( \frac{dz'}{v_{\text{drift}}(z')} \right).
\]

where the drift velocity is a function of distance. Assuming \( v_{\text{drift}} \sim 10 \text{ km s}^{-1} \) for the shock length \( L = 10^{15} \text{ cm} \), we can estimate the passage time as

\[
\tau_{\text{flow}} = \frac{L}{v_{\text{drift}}} = 30 \left( \frac{L}{10^{15} \text{ cm}} \right) \left( \frac{10 \text{ km s}^{-1}}{v_{\text{drift}}} \right) \text{yr}.
\]

To understand the effect of rotational excitation by gas bombardment, we need to compare the spin-up time by Gold stochastic torques is rather short
compared to the time passing the shock structure. Therefore, nanoparticles can be rotating suprathermally in a substantial fraction of the shock. The spin-up timescale is larger for larger grains, such as classical grains of \( a = 0.1 \mu m \), because \( \tau_{\text{spin-up}} \propto a \).

The rotational damping time is given by Equation (11), which corresponds to

\[
\tau_H \simeq 0.067a^{-3} \left( \frac{T_{\text{gas}}}{1000 \text{ K}} \right)^{-1/2} \left( \frac{n_H}{10^5 \text{ cm}^{-3}} \right)^{-1} \text{ yr}, \tag{37}
\]

which is long compared to the spin-up time (Equation (36)). Therefore, for supersonic drift, grains can be spun up to suprathermal rotation before the damping by gas collisions.

Rapidly spinning nanoparticles emit strong electric dipole radiation, which can also damp grain rotation on a timescale of

\[
\tau_{\text{ed}} = \frac{3f^2e^3}{\mu^2kT_{\text{gas}}} \simeq 225 \left( \frac{a^2}{3.8\beta} \right) \left( \frac{T_{\text{gas}}}{1000 \text{ K}} \right)^{1/2} \text{ yr}, \tag{38}
\]

where \( \mu \) is the dipole moment and \( \beta = \beta/(0.4D) \), with \( \beta \) being the dipole moment per structure of the grain (see Section 5), and the small contribution of dipole moment due to asymmetric charge distribution on the grain surface is ignored for numerical convenience (Draine & Lazarian 1998; Hoang et al. 2010).

Comparing \( \tau_{\text{ed}} \) with \( \tau_H \), one can see that, for hot and dense shocked regions, the electric dipole damping rate is lower than the gas damping rate. Thus, we expect that the excitation by gas collisions and neutral drift is very efficient in spinning nanoparticles up to extremely fast rotation because electric dipole emission is not fast enough to remove the grain angular momentum.

### 3.5. Grain Charge Distribution

In the shock code used for computing the shock structure, calculations of grain charge distribution are not yet included. Therefore, to find the grain charge distribution, we take the physical parameters of the shock as input parameters for our charging code (Hoang et al. 2011; Hoang & Lazarian 2012).

The temperatures \( T_{\text{c}}, T_{\text{i}}, T_{\text{c}}, T_{\text{g}} \), number density of neutrals, ion species, and ionization fraction \( (\xi_\text{H} \text{ and } \chi_\text{M}) \) at each location in the shock obtained from the shock model are used to find the collisional charging rate. Photoelectric emission is calculated as in Weingartner & Draine (2001; see also Hoang & Lazarian 2012), assuming a similar radiation spectrum to the ISRF, but with the strength \( \chi \) shown in Table 1.

Figure 4 shows the charge distribution of PAHs at different positions in the shock. For grains below 10 Å, the charge is mostly between \( Z = -1 \) and \( Z = 0 \), with a considerable probability on \( Z = -1 \). The fraction of grains being on the negative charge states increases with increasing \( a \), and it also varies with the distance in the shock. Since the neutral gas-charged grain drift is only relevant for charged grains, a high probability of being on \( Z = -1 \) indicates that grain excitation by neutral drift is important.

- Note that the collisional charging time is comparable to the mean time between two collisions with electrons, \( \tau_{\text{col}}/\tau_{\text{ed}} \sim 1 \text{ yr} \), which is much shorter than the flow time. Thus, we can find the charge distribution of nanoparticles in C-shocks.
Nanoparticles can indeed rotate suprathermally owing to supersonic neutral drift. The ratio $T_{\text{rot}}/n$ increases with grain size as a result of an increasing probability of being on the negative charge states. The ratio $T_{\text{rot}}/n$ also varies with the shock location and is larger inside the shock.

The rotation rate at the rotational temperature $T_{\text{rot}}$ is given by

$$\omega_{\text{rot}} = \frac{1}{2\pi} \left( \frac{3kT_{\text{rot}}}{I} \right)^{1/2} \approx 1.4 \times 10^{10} \tilde{\rho}^{-1/2} \omega^{-2/3} \left( \frac{T_{\text{rot}}}{10^3 \text{ K}} \right)^{1/2} \text{ Hz},$$

(42)

where $\tilde{\rho} = \rho/3$ g cm$^{-3}$. Thus, for $T_{\text{rot}} \gtrsim 10^3$ K, nanoparticles of $a = 1$ nm can rotate extremely fast at $\omega_{\text{rot}} \gtrsim 10^{10}$ s$^{-1}$.

4. Rotational Disruption for Extremely Fast Rotating Nanoparticles

4.1. Rotational Disruption

In this section, we introduce a new mechanism of dust destruction in shocks that is based on centrifugal stress within rapidly spinning nanoparticles, namely, rotational disruption.

The basic idea of rotational disruption is as follows. A spherical dust grain rotating at velocity $\omega$ develops a centrifugal stress due to centrifugal force, which scales as $S = \rho a^2 \omega^2/4$ (Hoang et al. 2019). When the rotation rate increases to a critical limit such that the tensile stress induced by centrifugal force exceeds the maximum tensile stress, the so-called tensile strength of the material, nanoparticles are disrupted.
instantaneously. The critical angular velocity for the disruption is given by

\[
\frac{\omega_{\text{crit}}}{2\pi} = \frac{1}{\pi a} \left( \frac{S_{\text{max}}}{\rho} \right)^{1/2} \\
\simeq 1.8 \times 10^{11} a^{-1/2} \rho^{-1/2} S_{\text{max},10}^{1/2} \text{ Hz},
\]

where \( S_{\text{max}} \) is the tensile strength of dust material and \( S_{\text{max},10} = S_{\text{max}}/10^{10} \text{ erg cm}^{-3} \) is the tensile strength in units of \( 10^{10} \text{ erg cm}^{-3} \).\(^7\)

The exact value of \( S_{\text{max}} \) depends on the dust grain composition and structure. Compact grains can have higher \( S_{\text{max}} \) than porous/composite grains. Ideal material without impurity, such as diamond, can have \( S_{\text{max}} \geq 10^{11} \text{ erg cm}^{-3} \) (see Hoang et al. 2019 for more details). In the following, nanoparticles with \( S_{\text{max}} \geq 10^{10} \text{ erg cm}^{-3} \) are referred to as strong materials, and those with \( S_{\text{max}} < 10^{10} \text{ erg cm}^{-3} \) are called weak materials.

Figure 7 shows the rms rotation rate \( \langle \omega^2 \rangle^{1/2} \) as a function of grain size. The critical disruption rate for the different tensile strengths is also shown for comparison. For instance, nanoparticles of size \( a < 0.8 \text{ nm} \) (marked by a red arrow) can be disrupted by the centrifugal force at \( S_{\text{max}} = 10^{10} \text{ erg cm}^{-3} \) with shock density \( n_H = 10^4 \text{ cm}^{-3} \) and shock velocity \( v_s = 20 \text{ km s}^{-1} \).

### 4.2. Disruption Rotational Temperature

From Equations (42) and (43) one can infer the rotational temperature required for grain disruption:

\[
T_{\text{rot}} \geq \left( \frac{32\pi a^2}{45k} \right) S_{\text{max}} \\
\simeq 1.6 \times 10^6 a^{-2/3} S_{\text{max},10} \text{ K}, \quad (44)
\]

An alternative unit of the tensile strength is dyne cm\(^{-2}\), but in this paper we use the units of \text{erg cm}^{-3} for \( S_{\text{max}} \).

\(T_{\text{rot}}\) is the rotational temperature required to disrupt grains. The critical rotational temperature for the disruption is important in shocked regions. Moreover, the disruption time scales as \( a^{2/3}\), thus, small nanoparticles tend to be disrupted faster than large grains.

### 4.3. Disruption Time and Critical Drift Velocity

Using the excitation coefficients obtained in Section 3.4, we can evaluate the time required to spin up nanoparticles to \( \omega_{\text{crit}} \), the so-called rotational disruption time, as follows:

\[
\tau_{\text{disr}} = \frac{J_{\text{crit}}^2}{(\Delta J)^2/(\Delta t)} = \frac{(I\omega_{\text{crit}})^2}{n_H m_H v_{\text{drift}}^3 \pi a^3} \\
\simeq 0.05 a^{4} n_5^{-1} S_{\text{max},10} \left( \frac{v_{\text{drift}}}{10 \text{ km s}^{-1}} \right)^{-3} \text{ yr}, \quad (45)
\]

where \( n_5 = n_H/(10^5 \text{ cm}^{-3}) \).

The disruption time is much lower than the flow time \( t_{\text{flow}} \) for a typical drift velocity of \( v = 10 \text{ km s}^{-1} \). Thus, rotational disruption is important in shocked regions. Moreover, the disruption time scales as \( a^4 \); thus, small nanoparticles tend to be disrupted faster than large grains.

For shock velocities of \( v_s < 50 \text{ km s}^{-1} \), the gas temperature is not high enough that thermal rotation can disrupt nanoparticles. As a result, to disrupt grains, one requires \( t_{\text{disr}} < \tau_{\text{fl}} \), which corresponds to

\[
v_{\text{drift}} \geq 9 a^{-1/2} \left( \frac{T_{\text{gas}}}{1000 \text{ K}} \right)^{1/6} S_{\text{max},10}^{1/3} \text{ km s}^{-1}. \quad (46)
\]

From Figures 2 and 3 one can see that the drift velocity in C-shocks can easily satisfy the above condition.

Figure 8 shows the critical drift velocity above which nanoparticles are disrupted, as a function of flow time. Several grain sizes and tensile strengths are considered. The critical velocity decreases rapidly with increasing flow time.
4.4. Disruption Grain Size

To calculate the smallest size \( a_{\text{min}} \) at which nanoparticles can withstand the rotational disruption, we compute \( \omega \) using the rotational temperature \( T_{\text{rot}} \) as given by Equation (41) at each shock location for a grid of grain sizes from 0.35 to 10 nm and compare it with \( \omega_{\text{cri}} \).

Figure 9 shows the obtained minimum size \( a_{\text{min}} \) as a function of distance in the shock for different values of \( S_{\text{max}} \) and three shock models. Strong nanoparticles can survive the shock passage (red line), while weak nanoparticles can be destroyed.

Grain disruption size increases toward the middle of the shock and then rapidly declines, which resembles the temperature and velocity profile of shocks (see, e.g., Figure 1). The disruption size is below 0.5 nm for the typical \( S_{\text{max},10} = 1 \), but it can be increased to 2.0 nm for weaker materials (see blue, orange, and green lines). The disruption size is largest for the shock model B (middle panel).

5. Spinning Dust Emission from Nanoparticles in C-shocks

To pave the way for future observations, in this section we will calculate spinning dust emission from nanoparticles in shocked regions, accounting for rotational disruption.

5.1. Spinning Dust Model

5.1.1. Electric Dipole Moment and Emission Power

The rotational emission mechanism is built on the assumption that nanoparticles have nonzero electric dipole moments. PAH molecules can acquire intrinsic dipole moments owing to polar bonds (see Draine & Lazarian 1998). The attachment of SiO and SiC molecules to the grain surface gives rise to the electric dipole moment for nanosilicates (Hoang et al. 2016).

Let \( N \) be the total number of atoms in a spherical nanoparticle of radius \( a \). Assuming PAHs with a typical structure \( \text{C:H} = 3:1 \) having mean mass per atom \( m \approx 9.25 \) amu, one obtains \( N_{\text{PAH}} = 545a^{3.7} \) for the mass density \( 4\rho_{\text{g}} m^{-3} \) (Draine & Lazarian 1998). Assuming nanosilicates with structure \( \text{SiO}_{4}\text{Mg}_{1.1}\text{Fe}_{0.9} \) having \( m = 24.15 \) amu, one has \( N_{\text{sil}} = 418a^{3.7} \) for \( 4\rho_{\text{g}} m^{-3} \) (Hoang et al. 2016).

Let \( \beta \) be the dipole moment per atom in the grain. Assuming that dipoles have a random orientation distribution, the intrinsic dipole moment of the grain can be estimated using the random walk formula:

\[
\beta = N^{2/3} \approx 86.5(\beta/0.4D)^{2}a^{3.7}D^{2}
\]

for PAHs and \( \mu^{2} \approx 66.8(\beta/0.4D)^{2}a^{3.7}D^{2} \) for nanosilicates (Hoang et al. 2016).

The power emitted by a rotating dipole moment \( \mu \) at angular velocity \( \omega \) is given by the Larmor formula:

\[
P(\omega, \mu) = \frac{2}{3} \frac{\omega^{2}\mu^{2} \sin^{2} \theta}{c^{3}},
\]

where \( \theta \) is the angle between \( \omega \) and \( \mu \). Assuming a uniform distribution of the dipole orientation, \( \theta \), then, \( \sin^{2} \theta \) is replaced by \( \sin^{2} \theta = 2/3 \).

5.1.2. Angular Momentum Distribution Function

In dense regions where gas–grain collisions dominate rotation dynamics of nanoparticles (e.g., in shocked regions), the grain angular velocity can be appropriately described by the Maxwellian distribution:

\[
f_{\text{MW}}(\omega, T_{\text{rot}}) = \frac{4\pi}{(2\pi)^{3/2}} \frac{\mu^{2}}{(kT_{\text{rot}})^{3/2}} \exp \left(-\frac{I\omega^{2}}{2kT_{\text{rot}}} \right),
\]

where \( I \) is the moment of inertia of the spherical nanoparticle of mass density \( \rho \) and \( T_{\text{rot}} \) is the grain rotational temperature.
5.1.3. Size Distribution: PAHs and Nanosilicates

Following Li & Draine (2001), nanoparticles are assumed to follow a lognormal size distribution:

\[
\frac{1}{n_H} \frac{dn_j}{da} = B_j \frac{a}{a_0} \exp \left( -0.5 \frac{\log(a/a_0)}{\sigma_j} \right)^2,
\]

where \( j = \text{PAH, sil} \) corresponds to PAHs and nanosilicate composition, \( a_0 \) and \( \sigma_j \) are the model parameters, and \( B_j \) is a constant determined by

\[
B_j = \frac{3}{(2\pi)^{3/2}} \frac{\exp(-4.5\sigma_j^2)}{\rho_\sigma a_0 \sqrt{2}} \times \left( \frac{m_X b_X}{1 + \text{erf}(3\sigma/\sqrt{2} + \ln(a/a_0)/\sigma) / \sqrt{2}} \right),
\]

where \( m_X \) is the mass grain per atom \( X \) and \( b_X = X_H Y_X \), with \( Y_X \) being the fraction of \( X \) abundance contained in very small sizes and \( X_H \) being the solar abundance of element \( X \). In our studies, \( X = \text{C} \) for PAHs and \( X = \text{Si} \) for nanosilicates. In addition, \( m_X = m_C \) for PAHs, and \( m_X = m(\text{SiO}_2\text{MgFe}) \) for nanosilicates of the adopted composition.

The peak of the mass distribution \( a^3dn_j/dn \) occurs at \( a_p = a_0 e^{3\sigma} \). Three parameters determine the size distribution of nanoparticles, including \( a_0, \sigma, Y_X \).

5.1.4. Spinning Dust Emissivity and Emission Spectrum

Let \( j_\nu(\mu, T_{\text{rot}}) \) be the emissivity from a spinning nanoparticle of size \( a \) at a location in the shock, where \( T_{\text{rot}} \) depends on local conditions in the shock (see Section 3). Thus,

\[
j_\nu(\mu, T_{\text{rot}}) = \frac{1}{4\pi} P(\omega, \mu) \rho(\nu, \mu) \frac{2\pi f_{\text{MW}}(\omega)}{\nu},
\]

where \( \rho(\nu, \mu) \) is the probability that the nanoparticle rotating at \( \omega \) emits photons at observed frequency \( \nu \), and the relation \( \omega = 2\pi\nu \) is assumed.

Here we disregarded the effect of grain wobbling (Hoang et al. 2010) and assume that nanoparticles are rotating along one axis as in Draine & Lazarian (1998). This assumption is likely appropriate for shocked regions because suprathermal rotation \( (T_{\text{rot}} \gtrsim T_{\text{gas}} \gg T_d) \) due to supersonic neutral drift is expected to induce rapid alignment of the axis of maximum inertia moment with the angular momentum (i.e., internal alignment; Purcell 1979).

The rotational emissivity per H nucleon is obtained by integrating over the grain size distribution (see Hoang et al. 2011):

\[
j_\nu(\mu, T_{\text{rot}}) = \int_{a_{\text{min}}}^{a_{\text{max}}} j_\nu(\mu, T_{\text{rot}}) \frac{1}{n_H} \frac{dn}{da} da,
\]

where \( dn/da = dN/da \) for spinning PAHs and nanosilicates, respectively.

The minimum size \( a_{\text{min}} \) at each location \( z \) in the C-shock is set equal to the disruption size (see Figure 9), which is a function of the shock velocity.

5.2. Spinning Dust Emissivity

We use Equation (53) to calculate the spinning dust emissivity at various locations inside the shock. The emissivity is calculated assuming that dust is composed of 90% PAHs and 10% nanosilicates. In the absence of rotation disruption, \( a_{\text{min}} \) is taken to be equal to 3.56 Å. When the rotational disruption effect is taken into account, \( a_{\text{min}} \) is determined as in Section 4. We fix the abundance of PAHs and nanosilicates throughout the shock, although their abundance should vary in the shock owing to grain shattering (Guillet et al. 2011).

Figure 10 shows spinning dust emissivity from nanoparticles computed at different location \( z \) in the shock. The black dashed line shows thermal dust emission from large grains (see Hoang et al. 2018b). When the rotational disruption effect is not taken into account, spinning dust emissivity is very strong and can peak at very high frequencies of \( \nu \sim 500 \) GHz for some locations (see panel (a)). When accounting for rotational disruption (panel (b)), both rotational emissivity and peak frequency are reduced significantly owing to the destruction of the smallest nanoparticles via rotational disruption. The effect
of rotational disruption is clearly demonstrated through the emission spectrum at locations $z = 5 \times 10^{15}$ cm and $z = 10^{16}$ cm, where the peak frequency is reduced from $\nu \sim 500$ GHz (panel (a)) to $\nu \sim 80$ GHz (panel (b)). In both cases, spinning dust is still dominant over thermal dust at frequencies $\nu < 100$ GHz (bottom panel).

### 5.3. Emission Spectral Flux

The spectral flux of spinning dust emission from nanoparticles in a spherical shocked region can be calculated as follows:

$$
F_\nu = \frac{L_\nu}{4\pi D^2} = \frac{1}{4\pi D^2} \int_V n_H dV \left( \frac{4\pi J_\nu}{n_H} \right)
$$

where $D$ is the distance from the shocked region to the observer, $V$ is the shock volume, and $z_i$, $z_f$ are the initial and final distances of the shock. Here $z_i = 10^{13}$ cm, and $z_f$ is also the shock length, determined by the shock distance where $T_{\text{gas}}$ decreases to the preshocked gas temperature.

Figure 11 shows the spectral flux for three shock models of different velocities, assuming nanoparticles made of strong material ($S_{\text{max}} = 10^{10}$ erg cm$^{-3}$). For this case, rotational disruption is quite inefficient for this case (see Figure 9). One interesting feature is that the emission spectrum consists of two parts: the first, low-frequency ($\nu < 100$ GHz) part with peak flux at frequency $\nu \sim 40$ GHz, and the second, high-frequency ($\nu > 100$ GHz) part with peak flux at $\nu \sim 300$–500 GHz. The second part is produced by the smallest nanoparticles that are excited to suprathermal rotation by supersonic neutral drift (see Figure 10 for emissivity). Furthermore, the peak flux decreases with increasing $n_H$ owing to the decreased shock length $z_f$ (see Figures 2 and 3).

Figure 12 shows similar results but for nanoparticles made of weaker materials such that rotational disruption is more efficient. Compared to Figure 11, one can see that the emission spectrum is similar to the first part of Figure 11, but the high-frequency peak is almost wiped out. The reason is that the smallest nanoparticles are significantly reduced owing to efficient rotational disruption, resulting in the suppression of the high-frequency part in the emission spectrum.

### 6. Discussion

#### 6.1. Dust Processing in Shocks: Comparisons of Rotational Disruption with Other Mechanisms

In shocked regions, shattering of large grains due to collisions between neutral and charged grains is suggested to produce PAHs and silicate nanoparticles, resulting in the modification of the original grain size distribution (Jones et al. 1996; Guillet et al. 2011). However, the lower cutoff of the resulting grain size distribution is arbitrarily chosen to be 5 Å in the previous studies.

On the other hand, thermal sputtering is believed to be a dominant process to destroy the smallest grains such as PAHs and nanoparticles in hot shocked regions. Let $Y_{sp}$ be the sputtering yield by a hydrogen atom bombarding on the dust grain at velocity $v_{\text{drift}}$. The sputtering rate is
which yields
\[
\frac{da}{dt} = \frac{n_H v_{\text{drift}} m_H Y_{\text{sp}}}{4 \rho} 
\approx \left( \frac{0.1 \mu m}{\text{yr}} \right) \left( \frac{v}{20 \text{ km s}^{-1}} \right) \beta m_H Y_{\text{sp}}. \tag{56}
\]

For the C-shock where the neutral drift velocity \( v_{\text{drift}} \ll 50 \text{ km s}^{-1} \) (see Figure 3), the sputtering yield is rather low, \( Y_{\text{sp}} < 10^{-3} \) (Draine 1995). Therefore, the destruction time for grains of radius \( a \) is given by
\[
\tau_{\text{sp}} = \frac{a}{\frac{da}{dt}} \approx 1.2 \times 10^3 \beta a^{-1} \left( \frac{20 \text{ km s}^{-1}}{v_{\text{drift}}} \right) \left( \frac{10^{-4}}{Y_{\text{sp}}} \right) \text{ yr}, \tag{57}
\]
where \( n_a = n_H/(10^4 \text{ cm}^{-3}) \). Comparing \( \tau_{\text{sp}} \) with \( \tau_{\text{disr}} \) (Equation (45)), we can see that the disruption time is much shorter than the sputtering time for \( a \) below several nanometers.

In this paper, we identified a new mechanism of destruction for nanoparticles in the shocks, namely, rotational disruption by stochastic mechanical torques. We showed that nanoparticles can be spun up to extremely fast rotation owing to high gas density, high temperature, and supersonic drift of neutrals relative to charged nanoparticles. As a result, nanoparticles are disrupted at some location in the shock where the tensile stress induced by centrifugal force exceeds the ultimate tensile strength. Physically, the high gas density and temperature due to shock compression allow gas collisional excitation to dominate over the electric dipole damping, making nanoparticles rotate at thermal angular velocities. Supersonic neutral drift then further drives nanoparticles to suprathermal rotation. The rotational disruption is quite efficient for weak nanoparticles. For strong nanoparticles of tensile strength \( S_{\text{max}} = 10^{10} \text{ erg cm}^{-3} \), small nanoparticles of \( a < 1 \text{ nm} \) (e.g., PAHs) are removed from the C-shock at \( v_i = 30 \text{ km s}^{-1} \). We find that nanoparticles of ideal material of \( S_{\text{max}} = 10^{11} \text{ erg cm}^{-3} \) cannot be destroyed in C-shocks with \( v_i \approx 30 \text{ km s}^{-1} \). Therefore, nanodiamonds produced in the previous stage of high-velocity shock by grain–grain collision (Tielens et al. 1987) would survive the shock and will be released in the ISM.

Table 2 summarizes the destruction mechanisms in the shocks and their characteristic timescales. The grain–grain collision timescale is estimated as the mean time between two collisions, \( \tau_{\text{gg}} = 1/(\pi a^2 n_{\text{gg}} v_{\text{drift}}) = 4/3 \pi a^2 / (3 n_H m_H v_{\text{drift}}) \).

### Table 2

| Mechanism                        | Timescales (yr) |
|----------------------------------|-----------------|
| Rotational disruption            | \( 0.5 a^{-4} n_{\text{HH}}^{-1} v_{\text{drift}}^{-1} S_{\text{max}}^{-1} \) \( ^a \)   |
| Thermal sputtering               | \( 3.1 \times 10^3 a^{-2} n_a^{-1} T_r^{-1/2} (10^{-4}/Y_{\text{sp}}) \) \( ^c \)         |
| Nonthermal sputtering            | \( 2.4 \times 10^3 a^{-2} n_a^{-1} v_{\text{drift}}^{-1} (10^{-4}/Y_{\text{sp}}) \) \( ^c \) |
| Grain–grain collision            | \( 7.6 \times 10^{-4} a^{-1} h_F^{-1} v_{\text{drift}}^{-1} \) \( ^c \)            |

#### Notes.

\( ^a \) \( v_{\text{drift}} = v_{\text{drift}}/(10 \text{ km s}^{-1}) \).  
\( ^b \) \( S_{\text{max}} = S_{\text{max}}/(10^{10} \text{ erg cm}^{-3}) \).  
\( ^c \) \( T_r = T_{\text{gas}}/(10^3 \text{ K}) \).

\[ 4\pi a^2 \frac{da}{dt} = n_{\text{HH}} v_{\text{drift}} \pi a^2 Y_{\text{sp}} m_H. \tag{55} \]
assuming the single size $a$ distribution with the gas-to-dust mass ratio $M_d/M = 100$. Moreover, thermal sublimation is obviously ineffective in dense regions with low radiation intensity considered in this paper. The rotational disruption appears to be the fastest mechanism to destroy nanoparticles in C-shocks. As a result, this mechanism would play an important role in constraining the lower cutoff of grain size distribution in dense C-shock molecular clouds.

It is noted that in the present study we assumed spherical shapes for nanoparticles and only considered the rotational excitation by stochastic mechanical torques. Realistic nanoparticles are expected to be irregular, such that the regular mechanical torques are shown to be stronger (Lazarian & Hoang 2007; Hoang et al. 2018a). As a result, the efficiency of mechanical disruption is perhaps more efficient than our present results.

### 6.2. Effect of Material Tensile Strength on Rotational Disruption

The tensile strength of dust grains and nanoparticles is very uncertain. Ideal material such as graphene has a highest tensile strength of $S_{\text{max}} \sim 1.3 \times 10^{12} \text{ erg cm}^{-3}$. If ideal PAHs can be considered as a sheet of graphene originating from collisions of graphite grains, then one can expect them to have a high tensile strength. Nevertheless, in astrophysical conditions, bombardment of energetic ions from cosmic rays can eject carbon atoms (see Micelotta et al. 2011), resulting in some defects. As a result, the tensile strength of PAHs can be reduced considerably, perhaps to $S_{\text{max}} \sim 10^9 \text{ erg cm}^{-3}$.

Nanosilicate, nanoiron, and nanodiamond particles can have high tensile strength. For example, the tensile strength of graphite is $S_{\text{max}} \sim 2 \times 10^{10} \text{ erg cm}^{-3}$ (MacMillan 1972). However, in shocked regions, nanoparticles can be heated to high temperatures of $T_g \sim 100 K$ owing to collisional heating (see Equation (25) in Tram & Hoang 2019). As a result, its tensile strength is expected to be reduced (K[reddi et al. 2016]. We show that nanoparticles with $S_{\text{max}} \lesssim 10^9 \text{ erg cm}^{-3}$ and size $a \lesssim 2 \text{ nm}$ would be disrupted in C-shocks, while stronger nanoparticles can survive the shock passage.

### 6.3. Implications for Mid-IR Emission from Shocked Regions

Most observations of supernova remnants do not show mid-IR PAH emission features ($\lambda = 3.3, 6.2, 7.7, 8.6,$ and $11.3 \mu m$; Smith et al. 2009), except observations for N132D by Tappe et al. (2006). Since PAHs are expected to be abundant in shocks owing to shattering of carbonaceous grains, the lack of PAH emission implies that PAH destruction is efficient in the shocked regions (see Kaneda et al. 2011 for a review). On the other hand, observations show ubiquitous mid-IR emission features (e.g., 11 and 21 $\mu m$), which are produced by hot very small grains ($a \sim 5–50 \text{ nm}$) stochastically heated by UV photons (Andersen et al. 2011).

We note that Micelotta et al. (2010) studied destruction of PAH molecules in interstellar shocks with velocity $v \sim 50–200 \text{ km s}^{-1}$. The authors found that PAHs are destroyed by sputtering due to proton and electron bombardment for $v > 100 \text{ km s}^{-1}$, but they can survive passing the shock at lower velocities.

In light of this study, small PAHs (i.e., $a < 1 \text{ nm}$) can be disrupted efficiently even at low shock velocities of $v < 50 \text{ km s}^{-1}$, but nanoparticles of $a \gtrsim 1 \text{ nm}$ can still survive the shock passage. Therefore, the proposed rotational disruption mechanism can successfully explain the lack of mid-IR PAH features and ubiquitous features at 9 and 21 $\mu m$ from very small grains (Rho et al. 2018).

### 6.4. Tracing Nanoparticles in Shocked Regions with Spinning Dust

PAHs and nanoparticles are expected to be abundant in shocked regions owing to grain–grain collisions (Jones et al. 1996; Guillet et al. 2011). Nevertheless, to date, there is no observational method available to test this top-down formation mechanism of nanoparticles. By modeling microwave emission from spinning dust, we show that spinning dust emission is very strong in shocked regions owing to rotational excitation by supersonic neutral drift. Even with a moderate abundance of Si or C in nanoparticles of $Y_C/Y_S = 5\%$, the spectral flux of spinning dust is still dominant over thermal dust at frequencies below 100 GHz. Spinning dust emissivity is several orders of magnitude higher than thermal dust when rotational disruption is disregarded.¹⁸

Therefore, future radio observations with ALMA and ngVLA will be used to probe nanoparticles and test the different dust destruction mechanisms in C-shocks.

### 6.5. Constraining the Shock Velocity in Dense Regions with Spinning Dust

C-shocks are ubiquitous in the ISM, especially in the dense, magnetized molecular clouds, due to the effect of jets from young stars. The popular technique to probe slow shocks is through molecular emission lines (CO, SiO, and H$_2$). Here we suggest a new technique to trace shocks using continuum microwave emission from spinning dust. This technique is based on the spinning dust mechanism, which is most suitable in shocked regions owing to highly rotational excitation by hot gas, supersonic neutral drift, and a high abundance of nanoparticles presumably formed by grain–grain collisions.

Figure 13 illustrates the variation of maximum emission flux (peak flux) of spinning dust emission spectrum with the shock velocity, which are obtained from Figures 11 and 12. The peak flux increases rapidly with shock velocity owing to both increased neutral drift velocity and higher gas temperature. The peak flux increases by a factor of 2 when the shock velocity increases from $v_s = 15$ to $30 \text{ km s}^{-1}$. In particular for model A ($n_H = 10^4 \text{ cm}^{-3}$), the peak flux increases significantly for $v_s \geq 20 \text{ km s}^{-1}$. For weak nanoparticles of $S_{\text{max}} = 10^9 \text{ erg cm}^{-3}$, there exists only one prominent peak (peak 1) because the second peak is destroyed as a result of the rotational disruption effect.

Figure 14 shows the peak frequency as a function of shock velocity. The first peak frequency increases with increasing $v_s$ for model A ($n_H = 10^4 \text{ cm}^{-3}$) only, but it slightly changes with $v_s$ for the other models (B and C) owing to the enhanced minimum size $a_{\text{min}}$ due to rotational disruption. On the other hand, the second peak frequency increases rapidly with $v_s$ for strong nanoparticles that are not disrupted by rotational disruption (top and middle panels).

¹⁸Note that the spinning dust emissivity for C-shocks is two orders of magnitude higher than in photodissociation regions (Hoang et al. 2010) if rotational disruption is not considered. In the absence of rotational disruption, the grain size distribution skewed to smaller sizes as in Guillet et al. (2011) would produce even stronger emissivity, which would be observed.
Magnetic fields play a crucial role in regulating shock structures in dense clouds (Draine 1980). Dust polarization resulting from grain alignment is a powerful technique to trace magnetic fields. To date, a detailed study of grain alignment in shocked regions is not yet available. We found that grains can be spun up to suprathermal rotation in shocks by stochastic torques. Grains of irregular shape also experience regular mechanical torques and can be aligned with the magnetic field (Lazarian & Hoang 2007; Das & Weingartner 2016; Figure 13. Emission flux of the first maximum (peak 1) and second maximum (peak 2) of emission spectrum vs. shock velocity for three different shock models, $n_H = 10^4 \text{ cm}^{-3}$, $n_H = 10^5 \text{ cm}^{-3}$, and $n_H = 10^6 \text{ cm}^{-3}$. Top, middle, and bottom panels show the results for three values of the tensile strength $S_{max}$. The peak flux increases rapidly with increasing $v_s$ until rotational disruption occurs.

6.6. Grain Alignment and Tracing Magnetic Fields in Shocks

Magnetic fields play a crucial role in regulating shock structures in dense clouds (Draine 1980). Dust polarization resulting from grain alignment is a powerful technique to trace magnetic fields. To date, a detailed study of grain alignment in shocked regions is not yet available. We found that grains can be spun up to suprathermal rotation in shocks by stochastic torques. Grains of irregular shape also experience regular mechanical torques and can be aligned with the magnetic field (Lazarian & Hoang 2007; Das & Weingartner 2016; Figure 14. Same as Figure 13, but for the peak emission frequency. The first peak frequency slightly changes with $v_s$ except for the model of $n_H = 10^4 \text{ cm}^{-3}$, but the second peak frequency increases rapidly with $v_s$. 

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Hoang et al. 2018a). If grains have iron inclusions that can greatly enhance its magnetic relaxation, grains can be aligned perfectly with the magnetic field (Hoang & Lazarian 2016a). Detailed studies of grain alignment and resulting dust polarization in shocks will be presented elsewhere in the near future.

7. Summary

We study rotational dynamics of nanoparticles in C-shocks of dense molecular clouds and discover a new mechanism of dust destruction by stochastic mechanical torques. Our principal results are summarized as follows:

1. For the first time, we study rotation dynamics of nanoparticles in C-shocks passing dense clouds, taking into account supersonic drift of neutral relative to charged nanoparticles. We find that charged nanoparticles can be rapidly spun up to suprathermal rotation by stochastic bombardment of gas atoms.

2. We find that suprathermally rotating nanoparticles can be rapidly disrupted into tiny fragments because the centrifugal stress induced by grain rotation can exceed the maximum tensile strength of grain material. Nanoparticles made of weak materials ($S_{\text{max}} \lesssim 10^7 \text{erg cm}^{-3}$) are easier to disrupt than nanoparticles of strong materials.

3. We compare the characteristic timescale of rotational disruption with other destruction mechanisms and find that rotational disruption is the most efficient mechanism in C-shocks with sufficiently large velocities. Thus, the minimum size of nanoparticles is constrained by the rotational disruption instead of thermal sputtering. This rotational disruption mechanism can play an important role in dust destruction in dense and hot regions compressed by supernova shocks and reverse shocks.

4. We perform modeling of microwave emission from rapidly spinning nanoparticles in C-shocks where the minimum size of nanoparticles is determined by rotational disruption. Even in the presence of rotational disruption, spinning dust emission is still dominant over thermal dust emission at frequencies $\nu < 100 \text{ GHz}$. We find that the peak frequency and emissivity increase with increasing shock velocity.

5. We suggest spinning dust emission as a new probe of nanoparticles and shock velocities in dense molecular clouds, where nanoparticles are expected to be abundant owing to grain–grain collisions and are rotating suprathermally owing to excitation by supersonic neutral drift.

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