A chip-based superconducting magnetic trap for levitating superconducting microparticles

Martí Gutierrez Latorre,1 Achintya Paradkar,1 David Hambraeus,1 Gerard Higgins,1,2 and Witlef Wieczorek1,*

1Department of Microtechnology and Nanoscience (MC2), Chalmers University of Technology, SE-412 96 Gothenburg, Sweden
2Institute for Quantum Optics and Quantum Information (IQOQI), Austrian Academy of Sciences, 1090 Vienna, Austria
(Dated: March 11, 2022)

Magnetically-levitated superconducting microparticles have been recently proposed as a promising platform for performing quantum experiments with particles in the picogram regime. Here, we demonstrate the superconducting technology to achieve chip-based magnetic levitation of superconducting microparticles. We simulate and fabricate a chip-based magnetic trap capable of levitating superconducting particles with diameters from 0.5 µm to 200 µm. The trap consists of two stacked silicon chips, each patterned with a planar multi-winding superconducting coil made of niobium. The two coils generate a magnetic field resembling a quadrupole near the trap center, in which we demonstrate trapping of a spherical 50 µm diameter SnPb microparticle at temperatures of 4 K and 40 mK.

I. INTRODUCTION

Superconducting levitation is a well known phenomenon and allows levitation of objects of vastly different masses [1]. In the context of quantum experiments with macroscopic objects [2], superconducting levitation can enable a novel experimental platform combining ultra-low mechanical dissipation of levitated particles [3–6] with the capability to stably trap micrometer-sized objects [7, 8]. Theoretical proposals to realize macroscopic quantum superposition states [9], as well as novel ultra-sensitive force and acceleration sensors [10, 11], have recently been put forward that exploit these unique features.

Recent experiments have shown initial steps in this direction by levitating micro-magnets on top of superconductors [12–16], diamagnetic particles in strong magnetic fields [4, 17, 18], and superconducting microparticles in millimeter-sized superconducting magnetic traps [19, 20]. Levitating a superconducting particle in a fully chip-based, microfabricated trap is advantageous as it enables high magnetic field gradients through miniaturization [21, 22] and a straightforward integration of precisely positioned superconducting circuits for read-out and quantum control of the particle’s motion [7–10].

In our work, we demonstrate a fully chip-based superconducting levitation platform. We discuss the design, simulation, and fabrication of our trap, and we use this trap in a proof-of-principle demonstration of levitating a 50 µm-diameter superconducting particle. We base the design of our trap on recent theoretical work in which different magnetic trap architectures were analyzed [7, 8, 23–25].

II. CHIP-BASED SUPERCONDUCTING MAGNETIC TRAP

A. Levitation requirements

In order to stably levitate a diamagnetic particle, first, a three-dimensional magnetic field minimum is required to confine it [24, 26]. The magnetic field distribution used to achieve such a confinement resembles that of an anti-Helmholtz coil configuration. At the levitation point, the magnetic force balances Earth’s gravity. Second, to initially lift the particle off the substrate, the magnetic lift force must also overcome adhesive forces between the particle and the substrate. From a simulation of our trap, we expect a lift force of 19 nN on a 50 µm-diameter superconducting sphere in the Meissner state when we apply a current of 0.5 A through the coils. This force greatly exceeds the particle’s weight (0.5 nN) and is, for certain particle-substrate interfaces, sufficient to overcome adhesive forces in our experiments. Note that these forces can be as large as 2 µN for a 50 µm metal sphere separated by 0.3 nm from a flat surface [27].

B. Design and simulation of the magnetic trap

The chip-based trap (see Fig. 1) consists of two multi-winding planar superconducting coils microfabricated on two silicon chips, which are stacked on top of each other. The coil separation is given by the 280 µm thickness of one silicon chip. Each coil has ten windings with 2 µm spacing, and each winding has a rectangular cross-section with 30 µm width and 1 µm thickness. The coils are made of niobium and can carry a maximal current of 0.9 A at 4 K, limited by the critical current density of niobium (3·10^10 A/m^2 [28]). The coil dimensions are chosen as a trade-off between the magnetic field strength and the microfabrication yield: Narrower windings with smaller
Figure 1. Chip-based magnetic trap. (a) Schematic of the trap assembly, showing two 280 μm thick silicon chips (top and bottom). The trap coils are colored in blue (bottom) and black (top), and the particle is shown between the coils. The colored rectangles indicate the orthogonal plane cuts used in Fig. 2. (b) False-color scanning electron microscope image of the top chip. The dark gray region is the hole where a particle is placed, the light gray region is the surface of the top silicon chip, and the yellow lines show the windings of the top coil. (c) Assembled two-chip magnetic trap. The bond pads on the chip (light blue) are wire-bonded using 25 μm diameter niobium wires (black lines). The crosses are alignment markers used for etching the hole in panel (b).

Figure 2. Simulated magnetic field strength in the trap scaled by the current in the coils, along the (a) xy, (b) yz, and (c) xz planes. The center of the bottom coil defines the origin of the coordinate system. The displacement of each cut plane from the origin is given at the top of each panel. The equilibrium position of the levitated 50 μm-diameter particle (black circle) is displaced from the origin along z due to gravity and along x due to the openings of the superconducting coils. Blue and black lines in (a) mark the projection of the bottom and top coil windings onto the xy slice, respectively.

Spacing can allow for a stronger magnetic field, due to the dependence of critical current density [28] and current uniformity [29, 30] on cross-section. However, millimeter-long narrow wires frequently detach from the substrate or break during assembly when their height to width ratio exceeds about 0.5.

To simulate the particle in the trap, we account for the three-dimensional geometry of the coils and the particle. We do this because the sample is not symmetric, thus, planar or rotationally symmetric two-dimensional models fail to capture its behavior, and also because the particle perturbs the trap field due to field expulsion [23, 24, 31]. We calculate the magnetic field distribution from finite element method simulations using COMSOL Multiphysics [32]. The simulations operate in the static regime and are based on the A-V formulation of the Maxwell-London equations [33], for details see Ref. [24]. The simulations yield the magnetic field distribution from finite element method simulations using COMSOL Multiphysics [32]. The simulations operate in the static regime and are based on the A-V formulation of the Maxwell-London equations [33], for details see Ref. [24]. The simulations yield the magnetic field (shown in Fig. 2), magnetic force and supercurrents. We assume that the particle is in the Meissner state and model it via the Maxwell-London equations in A-V formulation [24]. This situation holds when the particle is cooled below its critical temperature in zero field, and if the field near the particle stays below the first critical field of the material that the particle is made of, as is the case in our experiment. The coils are made of a type-II superconductor; we capture this in the model assuming a nearly-perfectly diamagnetic material (relative permeability 0.001) with a high electrical conductivity for the coils, as described in Ref. [30]. Hence, our model assumes that (i) the particle is in the Meissner state, and (ii) that there is no trapped flux in the levitated particle, inside the coil wire or inside the coil windings. Trapped flux would affect the levitation height, trap frequencies and mechanical dissipation.

Fig. 2 shows the trapping magnetic field, with a three-dimensional field minimum between the coils. The particle’s equilibrium position is slightly shifted along the z axis due to gravity, and along the x axis due to the openings of the coils.

The simulated magnetic field allows us to estimate the trapped particle’s centre-of-mass (COM) motional frequencies: We calculate the restoring force acting on the particle when it is shifted by a small distance from its equilibrium position [24]. In this way, we obtain motional frequencies for a 50 μm particle, $(\omega_x, \omega_y, \omega_z) = 2\pi (43 \pm 4.64 \pm 19, 125 \pm 3)$ Hz when 0.5 A current is passed through the coils (error is simulation uncertainty, see Ref. [24]). These frequencies are much lower than
the frequencies of typical micro- and nanomechanical resonators used in quantum experiments [34]. As a consequence, if the motional modes are in thermal states they will have around $10^9$ ($10^7$) phonons at 4 K (10 mK). Thus, in order for the levitated particle to be in its COM motional ground state additional cooling techniques, such as feedback [5, 6] or sideband cooling [35, 36], are required.

The magnetic trap can be used to levitate particles of a huge range of diameters; the lower limit depends on the London penetration depth, $\lambda_L$, and the upper limit depends on the first critical field strength of the particle, $B_{c1}$, or is given by the geometry of the trap. For example, SnPb particles with diameters from 500 nm to 220 $\mu$m could be levitated in our chip-based trap (assuming $\lambda_L = 100$ nm and $B_{c1} = 40$ mT [37, 38], when using a trap current of 0.5 A).

### III. SUPERCONDUCTING MICROPARTICLES

We use spherical microparticles made of lead (Pb) or a tin-lead alloy (Sn63Pb37), shown in Fig. 3, since lead and tin-lead have critical temperatures higher than 4 K (6.4 K and 7.0 K, respectively). Additionally, they have relatively high first critical field strengths (40 mT and 80 mT respectively [40]). We determined all these values, except for the critical field of lead, using AC magnetic susceptibility measurements.

The Pb microparticles are made in-house using ultrasonic cavitation [41], which yields near-spherical particles with a distribution of diameters between 0.5 $\mu$m and 200 $\mu$m. The tin-lead microspheres of 50 $\mu$m diameter are commercially available (EasySpheres).

### IV. EXPERIMENTAL SETUP

The chip trap is placed in a dilution refrigerator, which has a viewport that provides optical access to the sample stage. We use a custom-made microscope employing Köhler illumination to monitor the particle on a CMOS camera.

The trap current is supplied by an external current source, that passes through both pre-installed and...
custom-made wiring, as shown in Fig. 4. It is crucial to thermalize the wiring at each stage, to minimize the heat load at the sample stage. Pre-installed copper wires transport the current from room temperature to the 50 K stage, then a pre-installed superconducting BSCCO tape transports the current to the 4 K stage. At the 4 K stage the BSCCO tape terminates in gold-plated copper connectors, to which we clamp a copper-clad, formvar insulated, 190 µm twisted NbTi wire pair, which transports the current to the sample stage. At the sample stage, the NbTi wire is clamped to bulky Nb bond pads on the sample holder. At either end where the NbTi cable is clamped, the insulation and the cladding are removed to ensure a superconducting connection. The NbTi wire is wound and glued with GE-varnish around copper bobbins, which are attached to different stages for thermalization, as shown in Fig. 4. The chip trap contains microfabricated Nb bond pads [see Fig. 1(c)], which are electrically connected to the bulky Nb bond pads on the sample holder via 25 µm-diameter Nb wire bonds.

The sample is magnetically shielded (Fig. 4) by two open-top baskets made of layers of superconducting and ferromagnetic material: the sample holder lies within a shield made of niobium and Cryoperm, and the entire sample stage lies within a shield made of lead, aluminium and mu-metal.

V. DEMONSTRATION OF MAGNETIC LEVITATION

In Fig. 5 we show images of a SnPb particle in the magnetic trap at a temperature of 4 K (see also video material [42]). When we apply sufficient current to the trap, the particle levitates. This is evidenced by a sudden change of the particle position from its initial rest position [Fig. 5(a)], additionally the particle becomes blurred because of its oscillatory motion about the trap center [Fig. 5(b)]. The motional amplitude is strongly damped after 1 s [Fig. 5(c)]. After about 10 s the continuous illumination causes superconductivity to break and as a result the particle falls down [Fig. 5(d)]. When we do not shine light on the particle, we can levitate it for several days. We observe similar levitation results when using pure lead microparticles and also when the trap is operated at 40 mK (see also video material [42]).

We extract the particle’s motional frequencies from an analysis of the levitation video. To this end, we determine the time-dependent particle center by fitting an ellipse to the particle images and identify the center position of the ellipse with the position of the particle in the xy plane. A Fourier transform of this time-dependent motion yields the data in Fig. 6. We can clearly identify two dominant frequency components and attribute these to the COM motional modes along the x and y direction, \((\omega_x, \omega_y) = 2\pi \times (32 \pm 1.6, 60 \pm 1.8)\text{ Hz}\), respectively. The frequencies are in good agreement with the simulation results of \((\omega_x, \omega_y) = 2\pi \times (43 \pm 4.6, 44 \pm 19)\text{ Hz}\). We attribute the small discrepancy to the spatial misalignment between the bottom and top coils, as is visible in Fig. 5.

VI. CONCLUSION AND OUTLOOK

We have presented the design, simulation and fabrication of a chip-based superconducting magnetic trap
for levitating superconducting microparticles of diameters between 0.5 \( \mu \)m and 200 \( \mu \)m. We have demonstrated stable levitation of 50 \( \mu \)m-diameter superconducting particles in this trap at temperatures of 4 K and 40 mK. In the future, we will lower the particle’s motional dissipation rate by using a DC-SQUID magnetometer to detect the particle motion non-invasively and by improving the magnetic field shielding. These are crucial steps to eventually bring the particle’s COM motion into the quantum regime. Note that in an independent recent experiment, chip-based superconducting magnetic levitation of a superconducting microparticle has also been realized [43].

ACKNOWLEDGMENTS

We thank Thilo Bauch and Avgust Yurgens for insightful discussions. Further, we appreciate fruitful discussions with Joachim Hofer, Philip Schmidt, Stefan Minniberger, Michael Trupke, Markus Aspelmeyer and the other members of the EU Horizon 2020 project MaQSens. We are thankful for initial microfabrication support from David Niepce. We acknowledge funding from the Knut and Alice Wallenberg foundation through a Wallenberg Academy fellowship (W.W.), the Wallenberg Center for Quantum Technology (WACQT, A.P.) and support from Chalmers Excellence Initiative Nano. G.H. acknowledges support from the Swedish Research Council (grant no. 2020-00381). Sample fabrication was performed in the Myfab Nanofabrication Laboratory at Chalmers. Simulations were performed on resources provided by the Swedish National Infrastructure for Computing (SNIC) at Tetralith, Linköping University, partially funded by the Swedish Research Council through Grant No. 2018-05973.

[1] F. Moon and P. Chang, *Superconducting Levitation: Applications to Bearings and Magnetic Transportation*, A Wiley interscience publication (Wiley, 1994).
[2] M. Arnldt and K. Hornberger, Testing of the limits of quantum mechanical superpositions, *Nature Physics* **10**, 271 (2014).
[3] U. Delić, M. Reisenbauer, K. Dare, D. Grass, V. Vuletić, N. Kiesel, and M. Aspelmeyer, Cooling of a levitated nanoparticle to the motional quantum ground state, *Science* **367**, 892 (2020).
[4] Y. Leng, R. Li, X. Kong, H. Xie, D. Zheng, P. Yin, F. Xiong, T. Wu, C.-K. Duan, Y. Du, and et al., Mechanical dissipation below 1 muhz with a cryogenic diamagnetic levitated micro-oscillator, *Physical Review Applied* **15**, 024061 (2021).
[5] F. Tebbenjohanns, M. L. Mattana, M. Rossi, M. Frimmer, and L. Novotny, Quantum control of a nanoparticle optically levitated in cryogenic free space, *Nature* **595**, 378 (2021).
[6] L. Magrini, P. Rosenzweig, C. Bach, A. Deutschmann-Olek, S. G. Hofer, S. Hong, N. Kiesel, A. Kugi, and M. Aspelmeyer, Real-time optimal quantum control of mechanical motion at room temperature, *Nature* **595**, 373 (2021).
[7] O. Romero-Isart, L. Clemente, C. Navau, A. Sanchez, and J. I. Cirac, Quantum magnetomechanics with levitating superconducting microspheres, *Phys. Rev. Lett.* **109**, 147205 (2012).
[8] M. Cirio, G. K. Brennen, and J. Twamley, Quantum Magnetomechanics: Ultrahigh-Q -Levitated Mechanical Oscillators, *Physical Review Letters* **109**, 10.1103/PhysRevLett.109.147206 (2012).
[9] H. Pino, J. Prat-Camps, K. Sinha, B. P. Venkatesh, and O. Romero-Isart, On-chip quantum interference of a superconducting microsphere, *Quantum Science and Technology* **3**, 025001 (2018).
[10] M. T. Johnsson, G. K. Brennen, and J. Twamley, Macroscopic superpositions and gravimetry with quantum magnetomechanics, *Scientific Reports* **6**, 37495 (2016).
[11] J. Prat-Camps, C. Teo, C. Rusconi, W. Wieczorek, and O. Romero-Isart, Ultrasensitive inertial and force sensors with diamagnetically levitated magnets, *Physical Review Applied* **8**, 034002 (2017).
[12] M. Niemetz, W. Schoepf, J. T. Simola, and J. T. Tuoriniemi, The oscillating magnetic microsphere: a tool for investigating vorticity in superconductors and superfluids, *Physica B: Condensed Matter* **280**, 559 (2000).
[13] T. Wang, S. Lourette, S. O’Kelley, M. Kayci, Y. Band, D. Kimball, A. Sushkov, and D. Budker, Dynamics of a ferromagnetic particle levitated over a superconductor, *Physical Review Applied* **11**, 044041 (2019).
[14] C. Timberlake, G. Gasbarri, A. Vinante, A. Setter, and H. Ulbricht, Acceleration sensing with magnetically levitated oscillators above a superconductor, *Appl. Phys. Lett.* **115**, 224101 (2019).
[15] A. Vinante, F. Falleri, G. Gasbarri, A. Setter, C. Timberlake, and H. Ulbricht, Ultralow mechanical damping with meissner-levitated ferromagnetic microparticles, *Physical Review Applied* **13**, 064027 (2020).
[16] J. Gieseler, A. Kabencell, E. Rosenfeld, J. D. Schaefer, A. Safira, M. J. A. Schuetz, C. Gonzalez-Ballestero, C. C. Rusconi, O. Romero-Isart, and M. D. Lukin, Single-spin magnetomechanics with levitated micromagnets, *Phys. Rev. Lett.* **124**, 163604 (2020).
[17] B. R. Slezak, C. W. Lewandowski, J.-F. Hsu, and B. D’Urso, Cooling the motion of a silica microsphere in a magneto-gravitational trap in ultra-high vacuum, *New Journal of Physics* **20**, 065028 (2018).
[18] D. Zheng, Y. Leng, X. Kong, R. Li, Z. Wang, X. Luo, J. Zhao, C.-K. Duan, P. Huang, J. Du, M. Carlesso, and A. Bassi, Room temperature test of the continuous spontaneous localization model using a levitated micro-oscillator, *Phys. Rev. Research* **2**, 013057 (2020).
[19] B. van Waarde, *The lead zeppelin - a force sensor without a handle*, Ph.D. thesis, Universiteit Leiden, The Netherlands, geboren te Haarlem, Nederland (2016).
[20] J. Hofer, M. Aspelmeyer, et al. (2021), in preparation.
[21] J. Fortágh and C. Zimmermann, Magnetic microtraps for ultracold atoms, Reviews of Modern Physics 79, 235 (2007).

[22] V. Dikovsky, V. Sokolovsky, B. Zhang, C. Henkel, and R. Folman, Superconducting atom chips: advantages and challenges, The European Physical Journal D 51, 247 (2009).

[23] J. Hofer and M. Aspelmeyer, Analytic solutions to the Maxwell–London equations and levitation force for a superconducting sphere in a quadrupole field, Physica Scripta 94, 125508 (2019).

[24] M. G. Latorre, J. Hofer, M. Rudolph, and W. Wieczorek, Chip-based superconducting traps for levitation of micrometer-sized particles in the meissner state, Superconductor Science and Technology 33, 105002 (2020).

[25] C. Navau, S. Minniberger, M. Trupke, and A. Sanchez, Levitation of superconducting microrings for quantum magnetomechanics, Physical Review B 103, 174436 (2021).

[26] M. D. Simon and A. K. Geim, Diamagnetic levitation: Flying frogs and floating magnets (invited), Journal of Applied Physics 87, 6200 (2000).

[27] S. Alvo, P. Lambert, M. Gauthier, and S. Régnier, A van der Waals force-based adhesion model for micromanipulation., Journal of Adhesion Science and Technology 24, 2415 (2010).

[28] W. R. Hudson and R. J. Jirberg, Superconducting properties of niobium films, Vol. 6380 (National Aeronautics and Space Administration, 1971).

[29] K. Il’in, D. Rall, M. Siegel, A. Engel, A. Schilling, A. Semenov, and H.-W. Huebers, Influence of thickness, width and temperature on critical current density of Nb thin film structures, Physica C: Superconductivity 470, 953 (2010).

[30] E. F. Talantsev, A. E. Pantoja, W. P. Crump, and J. L. Tallon, Current distribution across type II superconducting films: a new vortex-free critical state, Scientific Reports 8, 1 (2018).

[31] Q.-G. Lin, Theoretical development of the image method for a general magnetic source in the presence of a superconducting sphere or a long superconducting cylinder, Phys. Rev. B 74, 024510 (2006).

[32] COMSOL AB, Stockholm, Sweden, Consol multiphysics 5.4, www.comsol.com (2019).

[33] A. M. Campbell, An introduction to numerical methods in superconductors, Journal of Superconductivity and Novel Magnetism 24, 27–33 (2011).

[34] M. Aspelmeyer, T. J. Kippenberg, and F. Marquardt, Cavity optomechanics, Reviews of Modern Physics 86, 1391–1452 (2014).

[35] J. Chan, T. P. M. Alegre, A. H. Safavi-Naeini, J. T. Hill, A. Krause, S. Gröblacher, M. Aspelmeyer, and O. Painter, Laser cooling of a nanomechanical oscillator into its quantum ground state, Nature 478, 89 (2011).

[36] J. D. Teufel, T. Donner, D. Li, J. W. Harlow, M. S. Allman, K. Cicak, A. J. Sirois, J. D. Whittaker, K. W. Lehnert, and R. W. Simmonds, Sideband cooling of micromechanical motion to the quantum ground state, Nature 475, 459 (2011).

[37] Y. Tsui, R. Mahmoud, E. Surrey, and D. Hampshire, Superconducting and mechanical properties of low-temperature solders for joints, IEEE Transactions on Applied Superconductivity 26, 10.1109/TASC.2016.2536806 (2016).

[38] J. M. Lock, Penetration of magnetic fields into superconductors iii. measurements on thin films of tin, lead and indium, Proceedings of the Royal Society of London. Series A. Mathematical and Physical Sciences 208, 391 (1951).

[39] W. Jaszczuk, H. J. M. t. Brake, J. Flokstra, D. Veldhuis, R. Stammis, and H. Rogalla, Bonding of a niobium wire to a niobium thin film, Measurement Science and Technology 2, 1121–1122 (1991).

[40] G. Chanin and J. P. Torre, Critical-field curve of superconducting lead, Phys. Rev. B 5, 4357 (1972).

[41] H. Friedman, Z. Porat, I. Halevy, and S. Reich, Formation of metal microspheres by ultrasonic cavitation, Journal of Materials Research 25, 633–636 (2010).

[42] M. G. Latorre, A. Paradkar, D. Hambraeus, G. Higgin, and W. Wieczorek, Video material at 10.5281/zenodo.5911190 for: A chip-based superconducting magnetic trap for levitating superconducting microparticles (2022).

[43] S. Minniberger and M. Trupke (2021), private communication.