Resistive Switching in Non-Stoichiometric Germanosilicate Glass Films Containing Ge Nanoclusters

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Received: 10 November 2020; Accepted: 7 December 2020; Published: 10 December 2020

Abstract: Metal–insulator–semiconductor (MIS) structures based on thin GeO[SiO2] and GeO[SiO] films on Si substrates were fabricated with indium-tin-oxide as a top electrode. The samples were divided into two series: one was left as deposited, while the second portion of MIS structures was annealed at 500 °C in argon for 20 min. The structural properties of as-deposited and annealed non-stoichiometric germanosilicate (GeSi x O y) films were studied using X-ray photoelectron spectroscopy, electron microscopy, Raman and infrared absorption spectroscopy, spectral ellipsometry, and transmittance and reflectance spectroscopy. It was found that the as-deposited GeO[SiO] film contained amorphous Ge clusters. Annealing led to the formation of amorphous Ge nanoclusters in the GeO[SiO2] film and an increase of amorphous Ge volume in the GeO[SiO] film. Switching from a high resistance state (HRS OFF) to a low resistance state (LRS ON) and vice versa was detected in the as-deposited and annealed MIS structures. The endurance studies showed that slight degradation of the memory window occurred, mainly caused by the decrease of the ON state current. Notably, intermediate resistance states were observed in almost all MIS structures, in addition to the HRS and LRS states. This property can be used for the simulation of neuromorphic devices and related applications in data science.

Keywords: germanosilicate glass; memristor; Ge nanoclusters; resistance states; thin films

1. Introduction

The development of information technologies requires devices for storing and processing huge amounts of information. Therefore, the creation of a universal storage device with a high speed of writing and reading information, along with a long storage time, high information capacity, and low operation power, is highly demanded in the field of nanoelectronics [1]. The capacity of memory matrices continues to grow while the planar integration of memory elements has almost reached its physical limits, which stimulates research of new physical principles and new materials for memory elements. In 1971, Leon Chua theoretically predicted the existence of the fourth element of electronics: a memory resistor, also called a memristor [2]. In 2008, Stanley Williams and his co-authors discovered
a memristor effect in a thin titanium oxide film, manifesting what “the missing memristor found” [3]. The memristor effect is based on the controlled switching of dielectrics to high and low resistance states (HRS and LRS, respectively). In 2013, Panasonic Semiconductor Solutions launched eight-bit MN101LR series microcontrollers with integrated, resistive random-access memories (ReRAMs) based on Ta$_2$O$_5$/TaO$_2$ double layers using 180-nanometer technology [4]. With a giant capacity of information storage in nonvolatile ReRAM, it is assumed that its energy consumption will be low. Presumably, only spintronic-based memory and ferroelectric RAM (FeRAM) can compete with ReRAM in energy consumption.

To date, the memristor effect has been observed in a wide class of different materials: perovskite films [5], organic films [6], fluorides and graphene oxides [7], high-k dielectrics such as TiO$_2$, HfO$_2$ [8], ZrO$_2$, Ta$_2$O$_5$ [9], Ta$_2$O$_{5-x}$/TaO$_{2-x}$ [10], Nb$_2$O$_5$, Al$_2$O$_3$, germanium oxides like GeO$_x$ [11], and silicon nitrides like SiN$_x$ [12]. It is especially important to develop memristors based on materials that are fully compatible with simple silicon planar technology, such as materials like silicon oxide SiO$_2$. The important advantage of non-stoichiometric germanosilicate glasses (GeSi$_x$O$_y$ solid alloys) are that the technology of their deposition is simple, inexpensive, and fully compatible with modern silicon technology [18]. These films are also interesting because they contain charge traps of various types. The nanoscale fluctuations of the potential in these solid alloys are due to the presence of SiO$_x$, GeO$_x$, Si, or Ge nano-inclusions. The bandgap values in SiO$_2$ (8–9 eV), GeO$_2$ (4.5 eV), and Ge (0.7 eV) differ significantly. The nano-inclusions of germanium oxides in silicon oxide are relatively shallow traps. Nano-precipitates with an excess of germanium atoms (or oxygen deficit regions) and Ge nanoclusters are quite deep traps.

Recently, there has been an increasing interest in materials with a low enthalpy of bonds between an atom of the fourth group of the periodic table of elements and an oxygen atom for the formation of memristors. This is because an easier formation of conductive filaments and their easier rupture in such materials are assumed. This softening should reduce the operation power for switching between the states, but it is also expected to reduce retention and endurance. On the one hand, softening can lead to the appearance of regimes of the intermediate resistance states (IRSs) in memristors. These states, supposedly, can be useful for the simulation of neuromorphic devices (e.g., stimulating synaptic plasticity and preliminary spike-enhanced plasticity) [19]. Multilevel resistance states in nanoscale neuromorphic devices with retention time satisfaction can be used as prospective artificial synapses [20].

2. Experiment

The samples of the non-stoichiometric germanosilicate glasses (i.e., GeSi$_x$O$_y$ solid alloys) were fabricated with a heating evaporation technique similar to the one previously described in [18]. After simultaneous evaporation of the GeO$_2$ and SiO$_2$ (or SiO) powders in a high vacuum (10$^{-8}$ Torr), deposition onto heavily doped n$^+$-type (resistivity 0.005 Ohm-cm) and p$^+$-type (resistivity 0.01 Ohm-cm) Si (001) substrates heated up to 100 °C occurred. The standard quartz microbalance method allowed for controlling the deposition rate at the level of ~0.1 nm/s. Two series of films were prepared by (1) evaporation of GeO$_2$ and SiO$_2$ powdered sources in accordance with the chemical composition, which we will refer to as GeO[SiO$_2$], and (2) evaporation of GeO$_2$ and SiO powdered sources in accordance with the chemical composition, marked as GeO[SiO] film. Note that, according to previous studies [21,22] on the condition of the evaporation of germanium dioxide powder, GeO$_x$ films of a composition very close to germanium monoxide (x ~ 1 ± 1.1) were deposited on the substrate. Presumably, this was due to the fact that germanium monoxide is a very volatile compound (i.e., it evaporates when an electron beam heats the targeted germanium dioxide powder and condenses on a cold substrate). The accompanying evaporating oxygen did not interact actively with the deposited film and practically did not oxidize germanium monoxide. The silicon substrates were cleaned in deionized water and dried. Thus, the growth of films was carried out on the native silicon oxide layer with a thickness of 2–3 nm. In addition, thick (~400 nm) reference samples were deposited on n-type
(10 Ohm-cm) Si (100) silicon and quartz substrates in the same deposition regimes for specific structural and optical studies.

The X-ray photoelectron spectra (XPS) were measured using the SPECS photoelectron spectrometer (Germany) with a PHOIBOS-150-MCD-9 hemispherical analyzer and a FOCUS-500 X-ray monochromator (AlK$_\alpha$ line, $h\nu = 1486.74$ eV, 200 W). The binding energy scale was previously calibrated by the position of the peaks of the core levels of the Au4f$_{7/2}$ (84.00 eV) and the Cu2p$_{3/2}$ (932.67 eV). The sample was mounted on double-sided copper conductive tape. For calibration, the C1s line (binding energy is 284.8 eV) from carbon, contained in hydrocarbons presenting on the surface of the samples, was used [23].

The JEM-2200FS transmission electron microscope (JEOL, Akishima, Japan) was used to investigate the structural properties of the samples. The high-resolution, cross-sectional transmission electron microscopy (HRTEM) mode was used, while the acceleration voltage was 200 kV. The Leica EM TXP target preparation device (Leica Microsystems, Mannheim, Germany) was used to prepare the cross-sectional samples by two-step mechanical polishing, followed by ion grinding.

It is known that analysis of vibrational spectroscopy data provides information about chemical bonds. The presence of nonpolar Ge–Ge bonds in the films was verified from analysis of the Raman spectroscopy data. Raman spectra were recorded at room temperature in the backscattering geometry by using an Ar$^+$ laser for excitation, whose wavelength was 514.5 nm, and the polarization of the laser irradiation was linear. A T64000 (Horiba Jobin Yvon) Raman spectrometer was used. The polarization of the scattered light was not analyzed. A liquid nitrogen-cooled, silicon-based charge-coupled device (CCD) matrix was used as the spectrometer’s photodetector, allowing a spectral resolution no worse than 2 cm$^{-1}$. The BX41 optical microscope accessory (Olympus, Tokyo, Japan) was used for the micro-scale recording of the Raman spectral data. To avoid local heating of the films by the laser beam, the sample was placed slightly further from the focus. The laser beam power on the sample was ~1 mW, while the spot diameter was ~20 µm. The polar Si–O and Ge–O bonds were studied using Fourier-transform infrared (FTIR) absorption spectroscopy. An FT-801 spectrometer (SIMEX analytical equipment, Novosibirsk, Russia) with a spectral resolution of 4 cm$^{-1}$ was used. As was mentioned earlier, for the FTIR analysis, the thicker (400 nm) reference films were deposited onto an n-type (resistivity 10 Ohm-cm) Si (001) substrate in the same growth condition.

The optical properties of the non-stoichiometric germanosilicate films in the visible region near the IR and ultraviolet (UV) regions were studied using spectral ellipsometry. An ELLIPS-1891-SAG (Institute of Semiconductor Physics, Novosibirsk, Russia) spectral ellipsometer was used for the ellipsometric analysis of the thin films on nontransparent silicon substrates [24]. The spectral dependencies of the ellipsometric angles $\Psi(\lambda)$ and $\Delta(\lambda)$ were measured in the range of 250–1100 nm. The spectral resolution of the device was about 2 nm, and the angle of light incidence was 70°. The four-zone measurement technique was used, and averaging over all four zones was performed. The SF-56 spectrophotometer (LOMO-Spectr, Saint Petersburg, Russia) was applied for the study of the transmission and reflection of light. The spectral resolution was better than 6 nm for the measurement range of 190–1100 nm. To record the reflection spectra, a PS-9 module (LOMO-Spectr, Saint Petersburg, Russia) was utilized. The angle of incidence was 9° with respect to the normal. The recorded spectra were normalized to the reference spectrum obtained for Si, with a natural oxide thickness of 3 nm like in previous works [25,26].

Square indium tin oxide (ITO) contacts (0.7 mm × 0.7 mm) with a thickness of 200 nm were deposited using magnetron sputtering. The layer resistance was 40 Ohm/τ, and the contact area was 0.5 mm$^2$. The metal–insulator–semiconductor (MIS) samples were divided into two series: the first portion of structures was left without annealing (as-deposited MIS), while the second series was further annealed at 500 °C for 20 min. The current–voltage (I–V) characteristics of the MIS structures were measured using a B2902A parameter analyzer (Agilent, Santa Clara, CA, USA) with a micro-probe station. The I–V measurements and positive and negative voltages were applied to the top ITO electrodes, while the back Si substrate electrodes had always been grounded. The equipment was
automated, which made it possible to measure the currents in ON and OFF states after the ON and OFF pulses, respectively, in order to investigate the endurance of the memristors.

3. Results and Discussion

3.1. Structural Studies

Figure 1 displays the XPS of the as-deposited thin GeO[SiO₂] and GeO[SiO] films. In addition to the survey XPS (Figure 1a), narrow spectral regions of the valence band (Figure 1b), Ge3d (Figure 1c), Si2p (Figure 1d), and O1s (Figure 1e) were measured. Survey spectra and individual spectral regions were obtained using the fixed analyzer pass energy of 50 eV and 20 eV, respectively. The survey spectra (Figure 1a) exhibited intense photoelectron peaks characteristic of germanium, silicon, oxygen, and carbon. No additional peaks belonging to other elements were found. The relative content of elements near the surface of the samples and the ratio of atomic concentrations were determined using the integrated intensities of photoelectron lines corrected for the corresponding atomic sensitivity factors, based on the Scofield’s calculations of the cross-sections [27]: 1.42 for Ge3d, 0.817 for Si2p, 1.0 for C1s, and 2.93 for O1s. As such, for the as-deposited thin GeO[SiO₂] sample, the O/Si ratio was 4.89, and the Ge/Si ratio was 1.43. For the GeO[SiO] sample, the O/Si ratio was 3.17, and the Ge/Si ratio was 1.04. The near-surface composition of the samples is presented in Table 1. It should be noted that the oxygen content in the near-surface region of the samples was found to be larger than assumed, according to the growth conditions (60% for GeO[SiO₂] and 50% for GeO[SiO]). This could have resulted from the oxidation of the near-surface region of the samples during their storage in the air atmosphere.

| Sample     | Ge, at.% | Si, at.% | O, at.% |
|------------|----------|----------|---------|
| GeO[SiO₂]  | 19.5     | 13.7     | 66.8    |
| GeO[SiO]   | 20.0     | 19.2     | 60.8    |

Figure 1c shows the spectra of the Ge3d region of the as-deposited samples. The binding energy of the most intense peak in both spectra was 32.8 ± 0.1 eV. This value is characteristic of germanium bound to four oxygen atoms, for example, in GeO₂ [23,28]. The low-intensity peak at ~31.2 ± 0.2 eV can be attributed to germanium in a non-stoichiometric oxide, GeOₓ [28]. In addition to the two indicated peaks, the shoulder with a lower binding energy at ~29.5 ± 0.1 eV was observed in the spectrum of the GeO[SiO] sample, which can be attributed to the germanium clusters (Ge–Ge bonds) [29]. Figure 1c also shows the result of the Ge3d spectra’s deconvolution into separate spectral components, carried out using XPS Peak 4.1 software [30], including the relative contents of Ge–O₄ (32.8 ± 0.1 eV), Ge–Ge₄ (29.5 ± 0.1 eV), and Ge–OₓGe₄₋ₓ (x = 1, 2, 3, 31.2 ± 0.2 eV) tetrahedrons. The Ge–OₓGe₄₋ₓ (x = 1, 2, 3) tetrahedrons actually should have appeared as three separate peaks, but they were not resolved in the spectra.

Figure 1d,e shows the spectra of the Si2p and O1s regions of the GeO[SiO₂] and GeO[SiO] samples, respectively. It was suggested that they were a superposition of the SiO + SiO₂ peaks in the Si2p spectra, and oxygen peaks arose from the germanium and silicon oxides in the O1s spectra. Detailed analysis of Figure 1a–e revealed that there were no Si–Si bonds (at least not in detectable quantities) in both samples, while Ge–Ge bonds were detected in the GeO[SiO] sample. This conclusion was confirmed by the analysis of the valence band spectra (Figure 1b), where the tails in the density of states propagating almost to zero binding energy could be observed, which was due to the GeOₓ inclusions in the films. The peak ~3 eV in the spectrum of GeO[SiO] was also due to Ge–Ge bonds.

The cross-sectional HRTEM images of the as-deposited samples are shown in Figure 2 (2a for GeO[SiO₂]) and 2b for (GeO[SiO]). Darker spots correspond to the Ge reach areas. It can be seen that only a few dark spots existed in the GeO[SiO₂] sample. They presumably correspond to the GeOₓ areas.
Remarkably, many dark spots can be seen in the GeO[SiO] sample. They presumably correspond to the amorphous Ge clusters [31] (a-Ge), with an average size of about 3 nm. The surfaces of both samples had very low values of surface roughness in the scale of 1 nm, which was controlled by an atomic force microscopy study of their surface topographies (See Figures S1 and S2 in Supplementary Materials).

Figure 1. X-ray photoelectron spectra (XPS) data of the as-deposited thin GeO[SiO2] and GeO[SiO] films. (a) Survey spectra; (b) valence band region; (c) Ge3d region; (d) Si2p region; and (e) O1s region.

Figure 3a displays the Raman spectra of both the as-deposited and annealed GeO[SiO2] and GeO[SiO] thin films, together with a reference spectrum measured from a virgin Si (001) substrate. For the as-deposited films as well as for the substrate, one could identify a peak at ~305 cm−1, which was due to two-phonon scattering on transversal acoustic phonons (2TA) [32]. This was because these thin films were semi-transparent. Thus, both the one-phonon scattering peak (520 cm−1) and two-phonon scattering peculiarity (2TA, ~305 cm−1) could be observed for the Si substrate. It should be noted that some asymmetry of the 520 cm−1 peak was due to Fano interference (interference of phonon and light hole-heavy hole scattering) in the p+ type heavily doped silicon [33]. In the spectrum of the
as-deposited GeO[SiO] film, one could observe a broad peak centered at about 275 cm⁻¹, which could be attributed to amorphous Ge [34]. One could see the growth of the intensity of this peak in the GeO[SiO] film and the appearance of this peak in the GeO[SiO₂] film after annealing. Therefore, annealing led to an increase of the volume of amorphous Ge nanoclusters in the GeO[SiO] film and to the formation of amorphous Ge nanoclusters in the GeO[SiO₂] film.

Figure 2. High-resolution transmission electron microscopy (HRTEM) cross-sectional image of the as-deposited thin films, (a) GeO[SiO₂] and (b) GeO[SiO].

Figure 3. (a) Raman spectra of the GeO[SiO₂] and GeO[SiO] thin films, measured before and after annealing at 500 °C for 20 min. A Raman spectrum from a virgin Si (001) substrate is also shown. (b) Fourier-transform infrared spectroscopy (FTIR) absorption spectra of the thick GeO[SiO₂] film (reference sample grown on a substrate not heavily doped with Si), measured before and after annealing. (c) FTIR absorption spectra of the thick GeO[SiO] film (reference sample grown on a substrate not heavily doped with Si), measured before and after annealing.

As it was assumed earlier [18,31,35], the a-Ge clusters appeared due to the following solid-state chemical reaction:

\[
\text{GeO} + \text{SiO} \rightarrow \text{Ge} + \text{SiO}_2.
\]

(1)

After annealing, the intensity of the a-Ge related peak increased in the GeO[SiO] film, which suggests that not all germanium monoxide had deoxidized during deposition, but part of it remained in the form of GeOₓ suboxides. It is known that GeOₓ is unstable and decomposes into germanium and germanium dioxide under annealing with temperatures higher than 300 °C [21,36].
Therefore, both annealed films consisted of a germanosilicate suboxide, which contained amorphous germanium (a-Ge) nanoclusters and possibly also a high concentration of oxygen vacancies.

It is known that the analysis of Si–O and Ge–O polar bond vibrations can provide information about the stoichiometry of SiO\(_x\) and GeO\(_x\) suboxides. Figure 3b,c shows the FTIR absorption spectra of the as-deposited and annealed thick GeO[SiO\(_2\)] and GeO[SiO] films (these samples were grown on a substrate not heavily doped with Si). The virgin n-type Si substrate with an electrical resistivity of 10 Ohm·cm was used as a reference when measuring the FTIR absorbance spectra. The spectra were dominated by a major line of approximately 1035–1075 cm\(^{-1}\), that was attributed to the Si–O–Si stretch mode in the SiO\(_x\) films [37,38]. Pai et al. [38] established that the position of this peak (in inverse centimeters) in SiO\(_x\) films almost linearly depends on the stoichiometric parameter \(x\), approximately expressed as

\[
\nu(\text{Si-O-Si stretching mode}) = 925 + 75x
\]  

The position of the Si–O–Si stretching mode peak in the as-deposited GeO[SiO] film (red curve, Figure 3c) was 1037 cm\(^{-1}\). Therefore, according to Equation (2), the stoichiometric parameter \(x\) in the as-deposited GeO[SiO] film was equal to 1.5. The position of the Si–O–Si stretching mode peak in the annealed GeO[SiO] film (blue curve, Figure 3c) was 1063 cm\(^{-1}\), so the stoichiometric parameter \(x\) in this case was equal to 1.85. Earlier it was supposed [39] that during deposition, not all germanium monoxide participates in a chemical redox such as Reaction (1), and by using the stoichiometric parameter \(x\) in the SiO\(_x\) part of germanosilicate solid alloys, one can determine the share of Ge clusters:

\[
\text{GeO} + \text{SiO} \rightarrow z\cdot\text{Ge} + (1 - z)\cdot\text{GeO} + \text{SiO}(1 + z)
\]  

Since the parameter \(z\) was equal to 0.5 in the as-deposited GeO[SiO] film, then about half of the germanium monoxide had been deoxidized in the chemical redox, shown in Reaction (1), during its deposition. In the annealed GeO[SiO] film, the parameter \(z\) was equal to 0.85, so about 85% of the germanium monoxide had been deoxidized in the chemical redox, show in Reaction (3), under deposition and subsequent annealing. As for the as-deposited and annealed GeO[SiO\(_2\)] films (black and green curve, Figure 3b), the positions of the Si–O–Si stretching mode peak were 1070 and 1075 cm\(^{-1}\), respectively. This suggests that the SiO\(_x\) inclusions in the germanosilicate solid alloy were close to stoichiometric silicon dioxide.

Other peaks visible in the GeO [SiO\(_2\)] films with a position of \(-990\) cm\(^{-1}\) (as-deposited film, black curve, Figure 3b) and \(-1000\) cm\(^{-1}\) (annealed film, green curve, Figure 3b) were due to the absorption of Ge–O–Si vibrations in the germanosilicate glass [31,39,40]. In addition to the Si–O and Si–O–Ge peaks, peaks associated with the stretching vibrations of the Ge–O bonds in all films [41,42] were seen. Like non-stoichiometric silicon oxide, the position of this peak (in inverse centimeters) in the GeO\(_x\) films almost linearly depended on the stoichiometric parameter \(x\) [42], as

\[
\nu(\text{Ge-O stretching mode}) = 743 + 72.4x
\]  

From the analysis of the Ge–O stretching mode position according to Equation (4), we can conclude that the stoichiometric parameter \(x\) in the GeO\(_x\) inclusions in the germanosilicate solid alloy was higher than 1.5. An important point is that, for both as-deposited films, one can observe a peak at about 3300 cm\(^{-1}\) due to the presence of O–H bonds in those films. The water could be either adsorbed on the surface of the films or contained in the voids of the as-deposited films. In the annealed films, the peaks related to water were much less intense. Thus, the annealing dried the films and presumably removed the voids by a densification process.

It is known that the density of electronic states determines the optical properties of materials; in particular, the mobility gap in dielectrics correlates with the optical gap in them [43]. Therefore, it is important to study the spectral dependence of the optical constants of dielectrics. For this, we used the methods of spectral ellipsometry and transmission and reflection spectroscopy, the results of which
are presented in Figure 4. Figure 4a,b shows the spectral dependencies of the complex refractive index, with its real part $n$ and the extinction coefficient (its imaginary part $k$) for the as-deposited thin GeO[SiO$_2$] and GeO[SiO] films, respectively. These data were obtained using ellipsometry angles $\Psi(\lambda)$ and $\Delta(\lambda)$ followed by determining the thickness and optical constants of the films from the model, considering one film on the substrate. The thickness of the GeO[SiO$_2$] film was determined to be 85 nm, and the thickness of the GeO[SiO] films was 64 nm. One can see that almost no absorption was registered in the GeO[SiO$_2$] film, which was related to the fact that the sensitivity of the method was insufficient to determine weak absorption. In the GeO[SiO] film, absorption was observed in the entire spectral range, with growth in the short wavelength edge. The refractive index of the GeO[SiO] film was larger than that of the GeO[SiO$_2$] film, due to the presence of a-Ge clusters in the first case. For estimation of the volume ratio of the Ge clusters in the solid alloy films, an effective medium approximation was used in the Bruggeman approach [44,45]. According to this approach, the volume ratio of a-Ge in the as-deposited GeO[SiO$_2$] film was less than 1%, and the volume ratio of a-Ge in the as-deposited GeO[SiO] film was about 10%. For the annealed films (ellipsometry data are not shown here), these ratios were 5% and 17.5% for the GeO[SiO$_2$] and GeO[SiO] films, respectively. These findings correlate with the Raman spectroscopy data (intensity of the broad 275 cm$^{-1}$ peak) in Figure 3a.

Figure 4. (a,b) Refractive index (its real part $n$) and extinction coefficient (imaginary part of refractive index $k$) of the as-deposited thick GeO[SiO$_2$] and GeO[SiO] films, respectively. (c,d) The sum of the transmission and reflection spectra of the as-deposited and annealed thick GeO[SiO$_2$] and GeO[SiO] films on quartz substrate, respectively. Separate transmission and reflectance spectra are shown in Figure S3 in Supplementary Materials.
It should be noted that it was not possible to apply a simple one-film-on-the-substrate model for the analysis of the spectral ellipsometry data of the annealed films. This was because annealing had led to the inhomogeneity of the non-stoichiometric germanosilicate films due to diffusion of the germanium atoms in the Si substrate [46].

The transmission and reflection spectroscopy data (shown in Figure 4c,d) confirmed the spectral ellipsometry results. Recall that the special reference samples on a quartz substrate in the same growth conditions were grown to measure absorbance. To avoid the features associated with interference, the sum of the transmittance and reflectance spectra are compared in Figure 4. One can see almost no absorption in the as-deposited GeO[SiO\textsubscript{2}] film in the visible and IR ranges (Figure 4c, black curve). The annealing led to the formation of a-Ge clusters in this film and, consequently, to the appearance of absorbance in the visible and IR ranges (Figure 4c, green curve). Since the as-deposited GeO[SiO] film had already contained a-Ge clusters, there was a clear absorbance in this film in the visible and IR ranges (the blue curve in Figure 4b and the red curve in Figure 4d). The annealing led to an increasing amorphous Ge volume in this film and, consequently, increased absorbance in the visible and IR ranges (Figure 4d, blue curve).

Therefore, all structural and optical methods confirmed the following statements. The as-deposited GeO[SiO] film contained a-Ge nanoclusters, while no such clusters were found in the as-deposited GeO[SiO\textsubscript{2}] film. Annealing led to an increase in the volume of a-Ge nanoclusters in the GeO[SiO] film and to the formation of a-Ge nanoclusters in the GeO[SiO\textsubscript{2}] film. All films contained Si–O and Ge–O bonds.

### 3.2. Studies of Resistivity Switching and Endurance

The schematic image of the MIS structures, energy band diagram, and the scheme of the endurance measurements are shown in Figure 5a–c, respectively. According to our previous studies [47], nanoscale fluctuations of electric potential in sub-oxides can play a considerable role in their electron transport. One of the significant advantages of germanosilicate solid alloys is that they offer the possibility to utilize these nanoscale fluctuations of the potential (i.e., parameters of the energy bands). The bandgap values in SiO\textsubscript{2} and GeO\textsubscript{2} differ significantly, being ~9 eV and ~5 eV, respectively. This difference allows modulation of the parameters of the traps consisting of germanium oxide inclusions in silicon oxide. Other possibilities to establish the nanoscale fluctuations of electric potential are based on the presence of suboxide areas, such as SiO\textsubscript{x} and GeO\textsubscript{x}, or on the formation of local areas with excess germanium atoms (which can possibly act as traps for both electrons and holes), as well as a-Ge nanoclusters. The valence band offset between crystalline Si and Ge is approximately ~0.5 eV, while the conduction band offset is only about ~0.1 eV (as shown in Figure 5b). Since the band offset for Ge is mainly in the valence band, a-Ge nanoclusters act as deep traps for holes rather than for electrons. It is important to note that the quantum size effect leads to a broadening of the bandgap in germanium nanoclusters (Figure 5b), so the larger the a-Ge nanocluster, the deeper the trap for electrons and holes. The band offsets for Si/GeO\textsubscript{2} heterojunctions are known [48]. Thus, yielding barriers for electrons and holes in such a system are about 1.2 eV and 3.3 eV, respectively. The corresponding barriers for Si/SiO\textsubscript{2} heterojunctions are also shown in Figure 5b. Unfortunately, the band offsets for Si/GeO heterojunctions are unknown.

The typical I–V characteristics of MIS structures grown on a p\textsuperscript{+}-type Si substrate are shown in Figure 6a–d. Switching from an HRS to an LRS (set) was seen at a positive voltage, and reverse switching from an LRS to an HRS (reset) was seen at a negative voltage. The set and reset voltages varied from +2 to +3.5 V and from ~2.5 to ~3 V for both as-deposited films (Figure 6a,c). It is worth noting that the current limitation was set during I–V measurements. Therefore, when the structures were switched to an LRS, the current value jumped, and a sharp decrease in the applied voltage was observed (Figure 6b). Insignificant fluctuations of the set and reset voltages of the films could be seen in the studied switching cycles. These results are similar to data obtained earlier using similar as-deposited MIS structures [18]. The ratio of currents in the ON and OFF states (the so-called memory
window) was rather low (about two to three orders of magnitude), but it should be noted that we carried out the measurements in an air atmosphere. In some cases, for the SiO₂-based memristor (with Si nanocrystals in SiO₂ film), the films did not show any switching effects when I–V measurements were carried out in an air atmosphere, while the high ON/OFF ratio was obtained only in a vacuum [15]. It is remarkable that no need to carry out the special forming procedure existed for our structures. This is a noteworthy benefit of our structures, in contrast with the structures reported previously by other authors (e.g., the memristors based on SiO₂ with Si nanocrystal films [15], or in the case of SiO₂ layers deposited by magnetron sputtering [49]). Our MIS structures on the p⁺-type Si substrates were forming-free. As one can see from Figure 6b,d, a considerably stable memristor effect was observed in both annealed films. However, in the case of the annealed GeO₂SiO₂-based MIS structure, a preliminary forming procedure with an applied voltage up to 5 V was required.

The endurance data are shown in Figure 7a–d for MISs grown on the p⁺-type Si substrate. The endurance measurement scheme is shown in Figure 5c. The various V_set and V_reset pulse values were applied to the MIS structures (the values are shown in Figure 7a–d) with a 5 ms pulse duration. V_read was always −1 V. One can see some degradation of the memory window for all MIS structures, mainly caused by a decrease in the ON current (Figure 7). Note that in almost all MIS structures, in addition to the HRS and LRS, the IRS was observed. The IRSs were not clearly distinguishable only in the annealed ITO/GeO₂SiO₂/p⁺-Si (001) structure (Figure 7d). The existence of IRSs can be of significant importance for the simulation of neuromorphic devices. The study of the effect of the pulse duration and amplitude on the switching processes (study of the so-called preliminary-spike-enhanced plasticity [19]) is the outlook for future experiments.

**Figure 5.** (a) Schematic image of the metal–insulator–semiconductor (MIS) structures. (b) The scheme of the corresponding energy band diagram. (c) The scheme of the measurements of endurance.
Attempts were made to estimate the energy needed to switch on and off the MIS structures and to normalize it to the contact area. It took a 5 ms long pulse of 4–6 V of voltage, with a maximal current up to 4 mA. The contact area was 0.5 mm\(^2\). It can be easily calculated that the energy density value was about 200 J/m\(^2\). If we assume that, in the future ReRAM matrix, the area of the element is 25 \(\times\) 25 nm, then the switching energy will be as small as \(-100\) fJ. It should be noted that these estimates were made without considering the influence of possible edge effects. However, it should be noted that the present structure was not optimized and the thickness of the dielectric was too large, while in a real application it should be to the order of 10 nm. Moreover, the switching pulse duration should be a few orders of magnitude smaller. Then, we can hope that the energy required for switching of one element (bit) will be less than 1 fJ, which is satisfactory for a memory element.

The contact-limited and volume-limited models were used in order to study the charge transport mechanism of the as-deposited films in an HRS and an LRS like in [18]. It should be remembered that local variations in the chemical composition of the layers of solid germanosilicate alloys led to local variations in the bandgap value (Figure 5b). Moreover, the local bandgap fluctuations led to the local electron potential fluctuations. The charge transport in a non-periodic fluctuating potential can be described according to the Shklovskii–Efros (S-E) percolation model [50]. This model assumes that excited electrons—that is, with an energy higher than the percolation energy level \(E_p\)—are delocalized and transfer the charges. In accordance with Equation (5), the \(j\) and \(F\) characteristics are exponentially dependent:

\[
j = j_0 \exp\left(\frac{-W - (C_e F a V_0^2) \gamma}{kT}\right)
\]

\(j_0\) is the preexponential factor, \(W\) is the switching energy, \(C_e\) is the capacitance per unit area, \(V_0\) is the percolation energy level, \(\gamma\) is the constant, \(k\) is the Boltzmann constant, and \(T\) is the temperature.

Figure 6. Current–voltage (I–V) characteristics of the MIS structures. (a) As-deposited ITO/GeO[SiO\(_2\)]/p\(^+\)Si (001) heterojunction; (b) Annealed ITO/GeO[SiO\(_2\)]/p\(^+\)Si (001) heterojunction; (c) As-deposited ITO/GeO[SiO]/p\(^+\)Si (001) heterojunction; and (d) annealed ITO/GeO[SiO]/p\(^+\)Si (001) heterojunction.
where \( j \) is the current density, \( F \) is the electric field intensity, \( j_0 \) is the pre-exponential factor, \( W \) is the percolation energy, \( a \) is the spatial scale of fluctuations, \( V_0 \) is the amplitude of the energy fluctuation, \( C \approx 0.25 \) is a numerical constant, and \( \gamma = 0.9 \) is a critical index. The percolation energy \( W \) and the pre-exponential factor \( j_0 \) determine the homogeneous vertical displacement of \( j \) (in a logarithmic scale, as in Figure 8). The spatial scale of the fluctuations and the amplitude of the fluctuation of energy \( V_0 \) determined the slope of the experimental data curve seen in Figure 8. As mentioned above, the simulation was carried out only in the enrichment mode for an Si substrate in order to disregard the contribution of the space charge region in the Si substrate.

![Figure 7](image_url)

**Figure 7.** The endurance characteristics of the MIS structures. (a) As-deposited ITO/GeO\[SiO\]\_2\]/p\(^+\)-Si (001) heterojunction; (b) Annealed ITO/GeO\[SiO\]\_2\]/p\(^+\)-Si (001) heterojunction; (c) As-deposited ITO/GeO\[SiO\]\_2\]/p\(^+\)-Si (001) heterojunction; and (d) annealed ITO/GeO\[SiO\]\_2\]/p\(^+\)-Si (001) heterojunction.

The comparison of the experimental results with the S–E percolation model (for the GeO\[SiO\]\_2\] film on the n\(^+\) and p\(^+\)-type substrates) was made earlier [18]. The charge transport in the as-deposited GeO[SiO] film on the n\(^+\)-type substrate was well described by the S–E model, as seen in Figure 8a, although slight deviations by the experimental data in the GeO[SiO] film on the n\(^+\)-type substrate from the S–E percolation model curve can be seen for low electric fields. The fitting parameters of the S–E model for GeO[SiO] were the following: \( j_0 = 5.1 \times 10^{21} \, \text{A/cm}^2 \), \( W = 1.5 \, \text{eV} \), \( V_0 = 1.8 \, \text{eV} \), and \( a = 2.8 \, \text{nm} \). From the change in the \( V_0 \times a \) value, it became possible to suggest that the composition of the GeO[SiO] film differed from the GeO[SiO\_2] film [18]. A considerably fine approximation of the experimental data for the GeO[SiO] film on the p\(^+\)-type Si substrate by the S–E percolation model can be seen in Figure 8b. The fitting parameters of the S–E model for GeO[SiO] in an HRS were the following: \( j_0 = 7.4 \times 10^{21} \, \text{A/cm}^2 \), \( W_{\text{HRS}} = 1.64 \, \text{eV} \), \( V_0 = 2.8 \, \text{eV} \), and \( a = 5 \, \text{nm} \). Meanwhile, the fitting parameters for GeO[SiO] in an LRS were as follows: \( j_0 = 7.4 \times 10^{21} \, \text{A/cm}^2 \), \( W_{\text{LRS}} = 1.53 \, \text{eV} \), \( V_0 = 2 \, \text{eV} \), and \( a = 3.5 \, \text{nm} \). The same \( V_0 \times a \) value in an LRS for the GeO[SiO] and GeO[SiO\_2] films on a p\(^+\)-type substrate indicate that the filaments had similar compositions [18]. In addition, the different \( V_0 \times a \) values in an HRS for GeO[SiO] and GeO[SiO\_2] correspond to the difference in their compositions [18].
The novelty of the present model is based on taking into account particles with a size of ~3 nm inside a 64–85 nm thin layer of germanosilicate glass, which builds 2020 Electronics related to optimization of the structure of the films in order to increase the ON/OFF ratio in resistance switching and to improve the endurance.

The standard room temperature was used for modeling in both the HRS and LRS cases. Since we used a slow voltage sweep to measure the I–V characteristics, the effects of the local temperature shifts in the percolation channels were not considered in the present study. Therefore, the real average temperature of the entirety of the structures was close to room temperature.

We highlight that switching to an LRS in our system took place due to the formation of the conducting filaments of oxygen vacancies (like in [15]) or oxygen multi-vacancies. The schematics of the proposed mechanism of the formation and rupture of these conducting filaments between electrodes via a-Ge nanoclusters are demonstrated in Figure 9. The absence of the need for forming has been demonstrated in the experiments (e.g., by applying a primary high positive voltage to the upper electrode). The bottom electrode, made of p⁺-Si, was grounded. No filaments (center image) could be observed in the absence of an external electric field. The essence of the proposed model lies in the organizing action of a-Ge particles with a size of ~3 nm inside a 64–85 nm thin layer of germanosilicate glass, which builds a conducting channel of oxygen vacancies even at a low voltage setting (one to the order of +2 V), leading to the formation of a conducting filament (shown in the right image). The absence of the forming stage reduced the time and the total energy consumption necessary for reaching the operating state of the memory element. At voltages of about ~3 V, a reset mode was observed (shown in the left image), after which the write–erase cycle of information in the memristor could be effectively repeated many times. The model is consistent with our recent experimental observations (Figures 5 and 6) and with earlier models for similar systems. The novelty of the present model is based on taking into account the organizing influence of a-Ge nanoclusters. The sink for oxygen ions during electromigration can not only be the bottom Si electrode, but also the Ge nanoclusters.

However, it should be noted that additional explanation of the resistive switching can be in the charging and discharging of the deep traps in the GeSiOₓ films. Charged traps, with their extra potential, change the flow conditions for electrons and holes in the S–E percolation model [51]. Such deep traps could be a-Ge nanoclusters. The distance between them exceeds the value favorable for sub-barrier tunneling (a few nm, as one can see in Figure 2). The LRS state can be achieved only if conducting filaments are formed between a-Ge clusters, as shown in Figure 9. Thus, the model of filament formation, in our opinion, is the main explanation for resistive switching. As a further outlook, the elucidation of this issue should be done. Other further directions of this research will be related to optimization of the structure of the films in order to increase the ON/OFF ratio in resistance switching and to improvement of the endurance.
The studied memristors can be used for the simulation of prospective neuromorphic devices.

4. Conclusions

Stable resistive switching was observed in MIS memristor structures based on non-stoichiometric germanosilicate (GeSi\textsubscript{3}O\textsubscript{y}) films with and without amorphous Ge nanoclusters. The prevailing mechanism of the observed resistive switching is the formation and rupture of conducting filaments. The formation and rupture of the filaments is caused by the electromigration of oxygen ions and oxygen vacancies. The endurance studies showed that some degradation of the memory window occurred for all structures, and it was mainly caused by a decrease of the ON current. In almost all MIS structures, intermediate resistance states (IRSS) were observed, in addition to the HRS and LRS. The studied memristors can be used for the simulation of prospective neuromorphic devices.

Supplementary Materials: The following are available online at http://www.mdpi.com/2079-9292/9/12/2103/s1.

Figure S1: The 2D AFM topography images of the GeO[SiO\textsubscript{2}] samples: (a) as-deposited; (b) annealed; Figure S2: Power spectral density (PSD) of roughness measured for fast scan axis direction X shows small values of object sizes (X-axis, nm\textsuperscript{2}) and amount of objects (Y-axis, \textmu m\textsuperscript{-1}) for the entire spectral range; Figure S3: Transmittance and reflectance curves for GeO[SiO\textsubscript{2}] and GeO[SiO] films on quartz substrates: left image—as-deposited films; right image—annealed films; Figure S4: Exemplary experimental I–V characteristics of the as-deposited GeO[SiO\textsubscript{2}]; Table S1: Roughness parameters of Si surfaces.

Author Contributions: Conceptualization, V.A.V.; formal analysis, G.N.K., A.A.G., G.K.K., I.P.P., I.A.A. and Z.F.; investigation, V.A.V., G.N.K., A.A.G., G.K.K., I.P.P., I.A.A., Z.F. and M.V.; project administration, P.G.; resources, M.V.; visualization, P.G.; writing—original draft, V.A.V.; writing—review and editing, P.G. All authors have read and agreed to the published version of the manuscript.

Funding: This work was supported by the Ministry of Education and Science of the Russian Federation, grant FSUS-2020-0029, while XPS and I-V curve analysis was done with financial support of the grant 075-15-2020-797 (13.1902.21.0024). The Raman spectroscopy and TEM were done on the equipment of CKP “VTAN” in the ATRC department of NSU.

Acknowledgments: The authors are thankful to Alexandre Bouché for help in growing the samples.

Conflicts of Interest: The authors declare no conflict of interest.

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Figure 9. Schematics of the formation (right) and rupture (left) of a conducting a-Ge-based filament in the GeSi\textsubscript{3}O\textsubscript{y} structure under the external electric field, taking into account the movement of oxygen ions and oxygen vacancies.
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