Electronic structure study of double perovskites

$A_2FeReO_6$ ($A$=Ba,Sr,Ca) and $Sr_2M$MoO$_6$

($M$=Cr,Mn,Fe,Co) by LSDA and LSDA+$U$

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Abstract

We have implemented a systematic LSDA and LSDA+$U$ study of the double perovskites $A_2FeReO_6$ ($A$=Ba,Sr,Ca) and $Sr_2M$MoO$_6$ ($M$=Cr,Mn,Fe,Co) for understanding of their intriguing electronic and magnetic properties. The results suggest a ferrimagnetic (FiM) and half-metallic (HM) state of $A_2FeReO_6$ ($A$=Ba,Sr) due to a $pdd$-$\pi$ coupling between the down-spin Re$^{5+}$/Fe$^{3+}$ $t_{2g}$ orbitals via the intermediate O $2p_\pi$ ones, also a very similar FiM and HM state of $Sr_2FeReO_6$. In contrast, a decreasing Fe $t_{2g}$ component at Fermi level ($E_F$) in the distorted Ca$_2$FeReO$_6$ partly accounts for its nonmetallic behavior, while a finite $pdd$-$\sigma$ coupling between the down-spin Re$^{5+}$/Fe$^{3+}$ $e_g$ orbitals being present at $E_F$ serves to stabilize its FiM state. For $Sr_2CrMoO_6$ compared with $Sr_2FeMoO_6$, the coupling between the down-spin Mo$^{5+}$/Cr$^{3+}$ $t_{2g}$ orbitals decreases as a noticeable shift
up of the Cr$^{3+}$ 3$d$ levels, which is likely responsible for the decreasing $T_C$ value and weak conductivity. Moreover, the calculated level distributions indicate a Mn$^{2+}$(Co$^{2+}$)/Mo$^{6+}$ ionic state in Sr$_2$MnMoO$_6$ (Sr$_2$CoMoO$_6$), in terms of which their antiferromagnetic insulating ground state can be interpreted. While orbital population analyses show that owing to strong intrinsic $pd$ covalence effects, Sr$_2$MMoO$_6$ ($M$=Cr,Mn,Fe,Co) have nearly the same valence state combinations, as accounts for the similar $M$-independent spectral features observed in them.

PACS numbers: 71.20.-b, 75.50.-y, 71.15.Mb
I. INTRODUCTION

A recent finding of the room-temperature tunnelling magnetoresistance (TMR) effect in double perovskites Sr$_2$FeMoO$_6$ (SFMO) and Sr$_2$FeReO$_6$ (SFRO) revives the study of 3$d$ ($M$) and 4$d$/5$d$ ($M'$) transition-metal oxide alloys $A_2MM'O_6$ ($A=$Ba,Sr,Ca). Most of the alloys have been up to now found to take a rock-salt crystal structure, an ordered one of the alternate perovskite units $AMO_3$ and $AM'O_3$ along three crystallographical axes. SFMO and SFRO taking this structure are predicted by band calculations to be a HM, where energy bands of one spin channel (up or down) cross $E_F$ and are therefore metallic but those of the other spin channel are separated by an insulating gap. Theoretically speaking, the conduction electrons are 100% spin polarized, this effect generally related to a ferromagnetic (FM) ordering of a (sub)lattice, despite a possible inter-sublattice antiferromagnetic (AFM) coupling in some cases. For the polycrystallic ceramics of SFMO and SFRO, an applied magnetic field can control magnetic domain reorientation and tends to parallelize the magnetization directions of FM domains and therefore reduces the spin scattering of spin-polarized carriers at grain boundaries, giving rise to a significant decrease of the measured resistivity. Such an effect was referred to as an interdomain/grain TMR. Like the well-known HM-like colossal MR manganites, the TMR materials also have potential technological applications to magnetic memory and actuators.

The MR materials with an interesting combination of electronic and magnetic properties are of current considerable interest also from the basic points of view. Double exchange (DE) model has been widely employed to account for the FM metallicity of La$_{1-x}$Ca$_x$MnO$_3$ and related compounds, in spite of its recent modification by taking into account a strong electron-phonon coupling arising from the Jahn-Teller splitting of the
Mn$^{3+}$ ions and even an alternative p-d exchange model as lately suggested for those O 2p-M 3d charge-transfer oxides. One DE-like mechanism was suggested for SFMO [SFRO] that a strong hybridization between the Mo$^{5+}$ (4d$^1$) [Re$^{5+}$ (5d$^2$)] and Fe$^{3+}$ (3d$^5$) down-spin $t_{2g}$ orbitals via a pdd-$\pi$ coupling leads to electron mobility being responsible for the HM behavior, and the itinerant down-spin carriers are antiferromagnetically polarized by the localized Fe$^{3+}$ S=5/2 full up-spins and therefore mediate a FM coupling in the Fe sublattice. Alternatively, very late a new mechanism was proposed that if the Fe sublattice has a FM ordering (being so actually), a bonding-antibonding splitting due to the Mo 4d [Re 5d]/Fe 3d hybridization results in a shift up (down) of the Mo 4d [Re 5d] $t_{2g}^\uparrow$ ($t_{2g}^\downarrow$) bands located between the Fe$^{3+}$ 3d full-filled $t_{2g}^\uparrow$ and empty $t_{2g}^\downarrow$ bands, and therefore an electron transfer from Mo [Re] $t_{2g}^\uparrow$ bands to $t_{2g}^\downarrow$ ones. This energy gain causes a negative spin polarization of the formally nonmagnetic Mo [Re] species, and the itinerant electrons in the partly filled $t_{2g}^\downarrow$ conduction bands cause kinetic energy gain further via the DE interaction, both of which commonly stabilize the FM state, as compared with the AFM or paramagnetic (PM) state.

In contrast, it was argued in another late study that a direct Re $t_{2g}$-Re $t_{2g}$ interaction is the main cause for the metallic behavior of Ba$_2$FeReO$_6$ (BFRO), and a lattice distortion of Ca$_2$FeReO$_6$ (CFRO) induced by the smaller-size Ca species disrupts the Re-Re interaction and makes itself nonmetallic. While magnetization measurements show that the latter has a higher $T_C$ value than the former, which seems surprising when referring to their distinct conduction behaviors.

One of the aims of this work is to probe which mechanism, either the direct or the indirect Re-Re interaction is essentially responsible for the conduction behavior of BFRO and SFRO by means of density functional theory (DFT) calculations. The present
results clearly show that the Re-O-Fe-O-Re interaction rather than the direct Re-Re one takes the responsibility. And it is suggested, based on the calculated orbital-resolved density of states (DOS), that a reduced Re $t_{2g}$-Fe $t_{2g}$ $pdd-\pi$ hybridization in distorted CFRO partly accounts for its nonmetallic behavior, compared with the cases of cubic BFRO and SFRO. While a presence of a finite Re $e_g$-Fe $e_g$ $pdd-\sigma$ hybridization in CFRO at $E_F$ contributes to its increasing $T_C$.

On the other hand, the dependence of the electronic, magnetic, and transport properties of Sr$_2$M$M_O$$_6$ ($M=$Cr,Mn,Fe,Co) on the 3$d$ transition-metal species is an intriguing issue. SFMO and Sr$_2$CrMoO$_6$ have a high $T_C$ value, and the former is a metallic compound while the latter is a nonmetal with a relatively low room-temperature resistivity. In contrast, Sr$_2$MnMoO$_6$ and Sr$_2$CoMoO$_6$ are AFM insulators. For the reason, DFT calculations are also designed for them. The valence states, spin moments, electronic and magnetic characters are discussed below in detail.

**II. COMPUTATIONAL DETAILS**

The structure data of $A_2$FeReO$_6$ ($A=$Ba,Sr,Ca) and Sr$_2$M$M_O$$_6$ ($M=$Cr,Mn,Fe,Co) are taken from Refs. 11, 2 and 8. These compounds have a cubic crystal structure except for the tetragonal Sr$_2$CoMoO$_6$ and monoclinic CFRO. An orthogonal cell is assumed for CFRO in order to simplify calculations, since the experimentally determined monoclinic cell ($\beta=90.02$) deviates slightly from an orthogonal one. FM calculations are performed for these compounds. As seen below, there is an induced negative spin polarization of the Re or Mo sublattice at the background of the FM Fe and/or Cr sublattices, which we call a FiM structure in this paper. In addition, the present FM solutions of Sr$_2$MnMoO$_6$ and
Sr₂CoMoO₆ can be extended to an explanation of their AFM insulating behaviors.

The full-potential linearly combined atomic-orbital (LCAO) band method, based on the local spin density approximation (LSDA) to DFT and on-site Coulomb correlation correction (LSDA+U), is adopted in the present calculations. Hartree potential is expanded in terms of lattice harmonics up to \(L = 6\), and an exchange-correlation potential of von Barth-Hedin type is adopted. The \(U (=3, 4, 4.5, 5 \text{ eV})\) parameters are used for the strongly correlated \(M (=\text{Cr, Mn, Fe, Co})\) 3\(d\) electrons, respectively; while a small \(U = 1 \text{ eV}\) for the weakly correlated Re 5\(d\) and Mo 4\(d\) electrons. Ba 5\(p5\)\(d6\)/Sr 4\(p4\)\(d5\)/Ca 3\(p3\)\(d4\)/s, M 3\(d4\), Re 5\(d6\)/Mo 4\(d5\), and O 2\(s2\)\(p\) orbitals are treated as valence states. 125 (64 for CFRO with a doubled cell) special \(k\) points in irreducible Brillouin zone are used in the present self-consistent calculations.

A description of the method for orbital population analyses is given below for the reason that a detailed discussion about the orbital occupation is made in the text.

A crystal wave function \(\Psi^k_j\) is expressed in terms of Bloch basis functions \(\{\Phi^k_l\}\) in the LCAO formalism:

\[
\Psi^k_j = \sum_l C^{kj}_l \Phi^k_l = \sum_l C^{kj}_l \frac{1}{\sqrt{N}} \sum_m e^{i\mathbf{k} \cdot (\mathbf{r} - \mathbf{r} - \mathbf{R}_m)} \phi_l(\mathbf{r} - \mathbf{r} - \mathbf{R}_m), \tag{1}
\]

where \(\phi_l\) denotes an atomic orbital wave function. \(k, j, l, N, \mathbf{R}_m, \) and \(\tau\) stand for, respectively, a wave vector, a band index, an atomic orbital label, number of unit cells, a lattice vector, and an atomic position.

The total DOS reads

\[
\rho(E) = \frac{1}{N_k} \sum_{kj} |\Psi^k_j|^2 \delta(E - E^k_j) = \frac{1}{N_k} \sum_{kj} C^{kj}_l C^{kj*}_{l'} S^{k}_{l'l} \delta(E - E^k_j) = \frac{1}{N_k N} \sum_{kj} \sum_{lmll'} C^{kj}_l C^{kj*}_{l'} < \phi_{l'} \phi_l | e^{i\mathbf{k} \cdot (\mathbf{r} + \mathbf{R}_m - \mathbf{r}' - \mathbf{R}_{m'})} \delta(E - E^k_j), \tag{2}
\]

where
\[ S_{l^l}^k = \langle \Phi_{l^l}^k | \Phi_{l^l}^k \rangle \] (3)

refers to an overlap matrix, and \( N_k \) represents the number of \( k \)-points.

\( \rho(E) \) can be decomposed into an on-site term \( \rho_A(E) (m=m' \text{ and } \tau=\tau') \) and an overlap term \( \rho_B(E) (m\neq m' \text{ or } \tau\neq \tau') \). The on-site term is written as

\[
\rho_A(E) = \frac{1}{N_k} \sum_{k_j} \sum_l \left| C_{l^l}^{k_j} \right|^2 \delta(E - E_{l_j}^k)
\] (4)

due to the orthogonality and normality of atomic orbitals at the same site. Correspondingly, the on-site occupation number \( Q_A \)

\[
Q_A = \int \rho_A(E) dE = \frac{1}{N_k} \sum_{k_j} \sum_l \left| C_{l^l}^{k_j} \right|^2
\] (5)

is composed of atomic contributions \( \{ \left| C_{l^l}^{k_j} \right|^2 \} \). Obviously, the sum rule for total number of electrons is not satisfied due to the non-orthogonality of atomic orbitals at different sites. For the reason, the overlap term \( \rho_B(E) \) is dealt with by Mulliken analysis\[^{14} \] which is widely used among quantum chemistry community and provides a reasonable description of local orbitals.

The overlap term is expressed as

\[
\rho_B(E) = \frac{1}{N_k} \sum_{k_j} \sum_{l,l',\neq l} C_{l^l}^{k_j} C_{l'^{l'}}^{k_j*} S_{l'^{l'}}^k \delta(E - E_{l_j}^k)
\]

\[= \frac{1}{N_k} \sum_{k_j} \sum_l \sum_{l',\neq l} \left| C_{l^l}^{k_j} \right|^2 \delta(E - E_{l_j}^k) + \left| C_{l'^{l'}}^{k_j*} \right|^2 \delta(E - E_{l'_j}^{k_j*}) + C_{l^l}^{k_j} C_{l'^{l'}}^{k_j*} S_{l'^{l'}}^k \delta(E - E_{l_j}^k)
\]

\[= \frac{1}{N_k} \sum_{k_j} \sum_l \sum_{l'} D_{l^l}^{k_j} \delta(E - E_{l_j}^k).
\] (6)

Mulliken analysis is taken such way that the overlap term is decomposed into atomiclike contributions \( D_{l^l}^{k_j} \), according to their respective ‘weight’ \( \left| C_{l^l}^{k_j} \right|^2 \).

As a result, one can calculate the orbital-resolved DOS and population, respectively, by the expressions
\[
\rho(E) = \rho_A(E) + \rho_B(E) = \frac{1}{N_k} \sum_{kj} \sum_l \left( |C^{kj}_l|^2 + D^{kj}_l \right) \delta(E - E^{kj}_l),
\]

(7)

\[
Q = \frac{1}{N_k} \sum_{kj} \sum_l (|C^{kj}_l|^2 + D^{kj}_l).
\]

(8)

Note that for a spin-polarized system, one can calculate the contributions from up- and down-spin channels and then obtain the values of spin moments.

III. RESULTS AND DISCUSSIONS

The LSDA calculations for BFRO and SFRO give a nearly same HM solution as recently reported for the latter.\[10\] Their level distributions are overall very similar, as is not surprising since, on one hand, both compounds have the same cubic structure except for a difference in their lattice constants 8.05 Å versus 7.89 Å;\[11\] on the other hand, two Ba\(^{2+}\)/Sr\(^{2+}\) ions per formula unit donate their four valence electrons, [all \(A(=\text{Ba},\text{Sr},\text{Ca})\) almost taking a valence state of +1.8 and a minor spin moment of −0.01 \(\mu_B\) in the present calculations], into \((\text{FeReO}_6)^{-4}\) unit and scarcely affect the valence bond interactions both in and between the \((\text{FeReO}_6)^{-4}\) units. Owing to the lattice distortion of CFRO—shrunk Fe-O-Re bond lengths and bent bond angles\[11\]—and therefore modified \(pdd\) hybridizations, however, a noticeable difference emerging in CFRO is that the down-spin \(e_g\) hybridized states are also present at \(E_F\). It can be seen in Fig. 1 that in \(A_2\text{FeReO}_6\) \((A=\text{Ba},\text{Sr},\text{Ca})\), the up-spin Fe 3\(d\) orbitals are almost full-filled, while the down-spin Fe 3\(d\) ones are nearly empty except for a small amount of occupations due to \(pd\) hybridizations, both of which indicate that the formal Fe\(^{3+}\) (3\(d^5\)) ions actually take a mixing 3\(d^5\) + 3\(d^6\)L state (L: a ligand hole) like an ordinary case, as also seen in Table I. Moreover, a small increase of Fe 3\(d\) population (and a corresponding minor decrease of Fe spin) as the change of
from Ca via Sr to Ba, being qualitatively in accord with the Mössbauer spectroscopy study\textsuperscript{11} indicates a decreasing oxidization of Fe, which is also supported by the calculated valence state of the coordinated oxygens, –1.47 for \(A=\text{Ca}\), –1.4 for \(A=\text{Sr}\), and –1.35 for \(A=\text{Ba}\). While a significantly strong \(pd\) hybridization effect is evident for the formal high valence \(\text{Re}^{5+}\) ions, which causes a larger bonding-antibonding splitting and a crystal-field \(t_{2g}-e_g\) splitting. As a result, although the down-spin \(\text{Re} t_{2g}\) states crossing \(E_F\) are partly occupied as the expected 2/3 filling, the \(5d\) orbital population is larger than 4 and far away from the formal \(\text{Re}^{5+} 5d^2\) as seen in Table I. A similar population difference larger than 2 also appears in the high valence oxides, \textit{e.g.}, \(\text{V}_2\text{O}_5\)\textsuperscript{20} and \(\text{NaV}_2\text{O}_5\)\textsuperscript{21} The relatively smaller \(\text{Re} 5d\) population in CFRO, compared with SFRO and BFRO, is also related to the relatively higher negative valence of the coordinated oxygens. A stronger ionicity of CFRO could be implied by a weaker Fe-O-Re covalence interaction caused by the bent Fe-O-Re bond angle. Moreover, a little smaller \(\text{Re} 5d\) population in SFRO than in BFRO could be due to a more delocalized behavior of the down-spin \(\text{Re} t_{2g}\) orbitals in SFRO, which is closely related to a larger band width caused by the smaller cubic lattice constant of SFRO.

As seen in Fig. 1, the \(\text{Re} t_{2g}\) levels exactly lie between the up- and down-spin Fe \(t_{2g}\) ones, and they are close to the down-spin Fe \(t_{2g}\) levels. As a result, the bonding-antibonding mechanism stated above induces a spin splitting of the \(\text{Re} 5d\) levels and a subsequent electron transfer and therefore a negative spin polarization. Moreover, it is evident that a stronger Re/Fe bonding-antibonding interaction occurs in the down-spin channel than in the up-spin one. The present LSDA calculations give the Fe (Re) spin moments of 3.72 (–0.99) \(\mu_B\) in BFRO, and 3.75 (–1.05) \(\mu_B\) in SFRO, and 3.76 (–1.07) \(\mu_B\) in CFRO, all of which are reduced by the \(pd\) hybridizations, compared with the ideal 5 (–
2) $\mu_B$ for Fe$^{3+}$ (Re$^{5+}$). A stronger Re 5$d$ spin polarization in SFRO than in BFRO could be due to a stronger bonding-antibonding mechanism in SFRO caused by the shorter Fe-O-Re bond. While the calculated largest Re spin in CFRO is ascribed to both an additional negative spin polarization of the Re $e_g$ electrons and weaker delocalization of the Re 5$d$ electrons. The calculated total spin, including both the weakly polarized oxygen spins with an averaged value of 0.05 $\mu_B$ and the minor $A$ spin, is accurately equal to 3 $\mu_B$ per formula unit as an expected integral value for a HM. While the reduced experimental values, e.g. 2.7 $\mu_B$ in Sr$_2$FeReO$_6$, are probably ascribed to a site-disorder effect as previously suggested. The calculated Fe spin moments agree well with the previous 3.7 $\mu_B$ in SFRO while the Re spin moments are larger than the corresponding value of $-0.78$ $\mu_B$. Although the previous values were calculated within relatively small radii (e.g., muffin-tin spheres) while the present ones are calculated for the magnetic ions with extended orbitals, it is not surprising that the Fe moments (nearly 75% spin-polarized) are almost identical because of the strong localization of the Fe 3$d$ orbitals. The present larger Re moments (about 50% spin-polarized) are ascribed to the delocalized Re 5$d$ orbital behavior.

A high Re-O (and Fe-O) covalent charge density is evident in Fig. 2. In addition, the up-spin Fe charge density is nearly spherical, which corresponds to the formal full-filled up-spin Fe$^{3+}$ 3$d$ orbital; while the down-spin Re (and Fe) density is obviously of the $t_{2g}$ orbital-like distribution. Moreover, the Re-Re interstitial densities visually arising from the O 2$p$ contribution almost have no difference between the up- and down-spin channels, which indicates that the net down-spin Re charge scarcely serves to the Re-Re interaction. In other word, the direct Re-Re interaction due to the itinerant down-spin Re $t_{2g}$ electrons is nearly impossible. Furthermore, the charge densities in the Re-O-Fe
bond are quite larger than the Re-Re interstitial densities. A combination of these results with the DOS shown in Fig. 1 leads to a suggestion that the down-spin Re \( t_{2g} \)-O 2\( p_\pi \)-Fe \( t_{2g} \) \( pdd-\pi \) coupling rather than the direct Re-Re interaction is responsible for the FiM and HM character of BFRO and SFRO.

In the calculated FiM and HM state of CFRO, however, the down-spin Fe \( t_{2g} \) component decreases at \( E_F \) due to bent Fe-O-Re bond angles. The reduced Fe-O-Re \( pdd-\pi \) coupling, as well as a little stronger site-disorder effect than in BFRO, could partly account for the nonmetallicity of CFRO. While a finite down-spin Re \( e_g \)-O 2\( p_\sigma \)-Fe \( e_g \) \( pdd-\sigma \) coupling emerges at \( E_F \) in CFRO, which is due to the \( t_{2g}-e_g \) mixing caused by the lattice distortion. The presence of such a coupling could stabilize the FiM state of CFRO and leads to its increasing \( T_C \) as compared with BFRO. However, the reasons for the nonmetallicity but high \( T_C \) of CFRO are not yet definitely clear.

The \( U \) correction lowers the occupied up-spin Fe 3\( d \) bands significantly and makes them much narrower and thus behave like a localized \( S=5/2 \) spin. The O 2\( p \) states undergo a noticeable change, while the Re 5\( d \) bands change insignificantly due to a weak electron correlation. The present LSDA+\( U \) results of SFRO are well comparable with those lately reported with a close value \( U_{eff} \approx 4 \) eV for Fe. The HM character remains unchanged, and particularly, the DOS at \( E_F \) [\( N(E_F) \)] caused mostly by the down-spin Re \( t_{2g} \)-O 2\( p \) hybridized states keeps the value of about 4 states/eV per formula unit (nearly twice as large as that of SFMO) as the above LSDA result, since the Re species are not strongly correlated ones. The LSDA+\( U \) calculations increase the Fe (Re) spin moments up to \( 4.16 \) (–1.22) \( \mu_B \) in BFRO, \( 4.22 \) (–1.27) \( \mu_B \) in SFRO, and \( 4.29 \) (–1.33) \( \mu_B \) in CFRO. The increases of the Fe spin moments are nearly twice as large as those of the Re moments, due to a stronger localization and electron correlation of the Fe ions. In addition, the
increasing difference between the present and previous LSDA+$U$ Re spin moments is ascribed to the $U=1$ eV correction to the Re 5$d$ states which is adopted in the present calculations but not in previous ones.}

Now we turn to Sr$_2$MMoO$_6$ ($M$=Cr,Mn,Fe,Co). First, the LSDA results of SFMO (see Fig. 3) are in good agreement with the previous ones. Like the above case of SFRO, the present Fe spin moment of 3.78 $\mu_B$ is almost identical with two independently calculated values of $3.79\mu_B$ and $3.73\mu_B$, and the Re spin moment of $-0.44\mu_B$ is larger than two corresponding ones of $-0.29\mu_B$ and $-0.30\mu_B$. These Re moments are all less spin-polarized ($<45\%$). These results suggest once again that the Fe spin is strongly localized while the Mo spin is delocalized. In SFMO the itinerant down-spin Mo $t_{2g}$ electrons mediate a FM coupling between the full Fe up-spins and are responsible for its HM character via the Mo-O-Fe coupling, like the above cases of BFRO and SFRO. Owing to the 4$d^1$ configuration of the formal Mo$^{5+}$ ions, $N(E_F)$ ($\approx 2$ states/eV per formula unit being consistent with the previous results) is reduced by nearly one half, compared with the above cases of BFRO and SFRO with Re$^{5+}$ 5$d^2$. It can be seen in Fig. 3 that besides a partial filling of the down-spin Mo $t_{2g}$ orbitals (formally 1/3 occupied), there is a quite large amount of Mo 4$d$ occupations between $-8$ and $-4$ eV due to strong $pd$ covalence effects. The Mo ions actually have a configuration nearly 4$d^{6.4}$ (see Table I).

For the case of Sr$_2$CrMoO$_6$, owing to a shift up of the Cr$^{3+}$ 3$d$ levels compared with the Fe$^{3+}$ case of SFMO, the down-spin Mo $t_{2g}$-O $p_\pi$-Fe $t_{2g}$ coupling is reduced around $E_F$, which could account for its decreasing $T_C$ and nonmetallic behavior (the latter as discussed above for CFRO). Besides, the occupied up-spin Cr$^{3+}$ $t_{2g}$ levels are very close to $E_F$ and near the empty up-spin Mo$^{5+}$ $t_{2g}$ ones. Thus the enhanced hybridization between them (also due to the relatively short Cr-O-Mo bond) leads to a broadened bandwidth,
which makes the up-spin $t_{2g}$ hybridized bands crossing $E_F$ also and partly occupied. The calculated Cr (Mo) spin moment is 1.67 (–0.65) $\mu_B$, and the total spin moment per formula unit is 1.13 $\mu_B$, which is increased by the following $U$ correction up to the expected 2 $\mu_B$ for an ideal FiM state. While an experimental magnetization value of $\approx 0.5 \mu_B$ is much smaller than these theoretical ones. A significant site-disorder effect could account for this large discrepancy since a minor difference between the ionic radii (Cr$^{3+}$ 0.615 Å, Mo$^{5+}$ 0.61 Å) most probably leads to a random structure. If a pair of antisite Cr/Mo ions leads to a decrease of spin moments by 6 $\mu_B$, according to the analyses in Ref. 22, the maximal antisite portion is estimated to be 25%. Note that the formal Mo$^{5+}$ ions take 4$d^{3.34}$ in the LSDA calculation. The Mo spin is larger in $\text{Sr}_2\text{CrMoO}_6$ than in SFMO, reflecting a weaker itineracy of the Mo $t_{2g}$ electrons in the former, which qualitatively accords with its nonmetallic behavior and lower $T_C$.

For $\text{Sr}_2\text{MnMoO}_6$, its lattice constant is larger than SFMO by $\approx 0.12$ Å and the Mn-O bond is quite long which indicates that the Mn ion most probably takes a high-spin bivalence state ($\text{Mn}^{2+}, S=5/2$) with a large ionic radius. Another evidence to support this argument is that there is no Jahn-Teller lattice distortion in $\text{Sr}_2\text{MnMoO}_6$ as expected for the $e_g$ half-filled Mn$^{3+}$ manganites. Owing to the Mo 4$d$-O 2$p$-Mn 3$d$ hybridizations, however, the broadened up-spin Mn $e_g$ bands cross $E_F$ and thus become partly occupied, and so do the down-spin Mo$^{6+}$ $t_{2g}$ bands, as shown by the present LSDA FM calculation. For $\text{Sr}_2\text{CoMoO}_6$, the LSDA FM calculation gives a HM solution, which is caused by the 2/3 filled down-spin Co$^{2+}$ $t_{2g}$ orbitals mixed with the O 2$p_x$ and Mo$^{6+}$ $t_{2g}$ ones. Experimentally, the $c$-axis Co-O bond is a little elongated in tetragonal $\text{Sr}_2\text{CoMoO}_6$ by 0.045 Å which lifts the triple-fold degeneracy of the Co $t_{2g}$ levels and splits them into a lower-energy doublet ($xz/yz$) and a higher singlet ($xy$). While only the weak
distortion seen by the Co $t_{2g}$ electrons, as shown by the LSDA calculation, is insufficient to open an insulating gap between the doublet and singlet. Instead the electron correlation determines the gap as seen below.

By comparison of the down-spin Mo $t_{2g}$ level positions near $E_F$, it is suggested that Mo takes Mo$^{5+}$ in Sr$_2$CrMoO$_6$ and Sr$_2$FeMoO$_6$ but Mo$^{6+}$ in Sr$_2$MnMoO$_6$ and Sr$_2$CoMoO$_6$. The Mo$^{6+}$ state in the latter two is also implied by the shrinked Mo-O bond length. While the finite Mo component at $E_F$ in Sr$_2$MnMoO$_6$ and Sr$_2$CoMoO$_6$ is entirely ascribed to the $pdd$ hybridizations.

As seen in Table I, however, the Mo 4$d$ population varies insignificantly in Sr$_2$M$\text{MoO}_6$ ($M=$Cr,Mn,Fe,Co) due to strong intrinsic $pd$ covalency effects, and correspondingly, the $M$ 3$d$ population increases by a step of $\sim 1$, suggesting nearly same valence states of all $M$. In addition, Sr and O retain the valence states of approximately $+1.8$ and $-1.4$ respectively, for all $M$. These results should be indicative of nearly a uniform valence state combination in Sr$_2$M$\text{MoO}_6$. Thus the present calculations support a previous suggestion that the $M$-independent spectral feature observed in Sr$_2$M$\text{MoO}_6$ at $\sim 2$ eV is ascribed to the O 2$p$-Mo 4$d$ transition. In addition, the relative spectral intensity can be qualitatively explained in terms of the varying numbers of the empty Mo $t_{2g}$ states. It can be seen in Fig. 3 that the down-spin Mo $t_{2g}$ orbitals at $E_F$ have nearly the same partial filling in Sr$_2$CrMoO$_6$ and Sr$_2$FeMoO$_6$, while they are almost unoccupied in Sr$_2$MnMoO$_6$ and Sr$_2$CoMoO$_6$. Moreover, the number of the Mo $t_{2g}$ holes is larger in Sr$_2$CoMoO$_6$ than in Sr$_2$MnMoO$_6$. These results account for nearly the same O 2$p$-Mo 4$d$ spectral feature of Sr$_2$CrMoO$_6$ and Sr$_2$FeMoO$_6$, the more intensive one of Sr$_2$MnMoO$_6$, and the most intensive one of Sr$_2$CoMoO$_6$.

The LSDA+$U$ calculation causes nearly the same changes for SFMO as for BFRO and
SFRO. The Fe (Mo) spin moment is increased up to 4.23 (–0.60) \( \mu_B \). The present values are larger than the lately reported ones of 3.97 (–0.39) \( \mu_B \) and they are in good agreement with experimental ones of 4.2 (–0.5) \( \mu_B \). For \( \text{Sr}_2\text{CrMoO}_6 \), the up-spin Cr \( t_{2g} \) bands shift downward and scarcely contribute to \( N(E_F) \), and the Cr spin moment is increased up to 2.42 \( \mu_B \). The down-spin Mo \( t_{2g} \) orbitals are rather weakly hybridized with the Cr \( t_{2g} \) ones, and they form conduction bands crossing \( E_F \), which could be responsible for its relatively low room-temperature resistivity. The present calculations are not sufficient to reproduce the nonmetallic behavior of \( \text{Ca}_2\text{FeReO}_6 \) and \( \text{Sr}_2\text{CrMoO}_6 \), and therefore a better description of their nonmetallicity could resort to the site-disorder effects in them. For \( \text{Sr}_2\text{MnMoO}_6 \), the up-spin Mn \( e_g \) and down-spin Mo \( t_{2g} \) bands contribute quite little to \( N(E_F) \) due to broadened bandwidths caused by the hybridization effects. The Mn spin moment of 4.54 \( \mu_B \) indicates the high-spin Mn\(^{2+} \) \((3d^5)\) state with \( S=5/2 \), and a minor Mo spin moment of 0.04 \( \mu_B \) suggests the formal Mo\(^{6+} \) \((4d^0)\) state. This minor but positive Mo spin is induced by a little stronger hybridization between the up-spin Mn \( e_g \) and Mo \( e_g \) orbitals. In terms of the Mn\(^{2+}/\text{Mo}^{6+} \) model, an AFM ground state can be interpreted by superexchange interactions via Mn-O-Mo-O-Mn bonds. Correspondingly, the hybridized bandwidths shown in the above FM calculations will be strongly suppressed in the AFM state, thus giving an insulating gap. Thus the AFM insulating ground state of \( \text{Sr}_2\text{MnMoO}_6 \) is reasonably explained. For \( \text{Sr}_2\text{CoMoO}_6 \), the electron correlation opens an insulating gap between the down-spin Mo \( xz/yz \) doublet and \( xy \) singlet. The Co spin moment of 2.93 \( \mu_B \) indicates a high-spin Co\(^{2+} \) \((3d^7, S=3/2)\) state. The calculated small and negative Mo\(^{6+} \) \((3d^0)\) spin moment of –0.12 \( \mu_B \) is ascribed to the stronger hybridization with the down-spin Co \( xz/yz \) doublet. Like the case of \( \text{Sr}_2\text{MnMoO}_6 \), this Co\(^{2+}/\text{Mo}^{6+} \) combination also leads to a superexchange-coupled AFM and insulating ground state of
**IV. CONCLUSION**

A systematic electronic structure study of $A_2FeReO_6$ ($A$=Ba,Sr,Ca) and $Sr_2M MoO_6$ ($M$=Cr,Mn,Fe,Co) has been performed by employing LSDA and LSDA+$U$ calculations.

(1) It is demonstrated that the HM character of BFRO, SFRO, and SFMO is not caused by the direct $M'$-$M'$ ($M'$=Re or Mo) interactions but the indirect $M'$-O-Fe-O-$M'$ $pdd$-$\pi$ couplings which are simultaneously responsible for their FiM character.

(2) It is suggested that a finite $pdd$-$\sigma$ hybridized state being present at $E_F$ in distorted CFRO contributes to its increasing $T_C$ value, compared with the case of BFRO.

(3) The reduced $pdd$-$\pi$ coupling in CFRO and $Sr_2CrMoO_6$, as well as the site-disorder effect, could account for their nonmetallic behaviors.

(4) The calculated level distributions and spin moments indicate the $M^{3+}$/Mo$^{5+}$ state for $Sr_2CrMoO_6$ and $Sr_2FeMoO_6$ but the $M^{2+}$/Mo$^{6+}$ state for $Sr_2M nMoO_6$ and $Sr_2CoMoO_6$, in terms of which both the itinerant FiM state of the former two and the superexchange-AFM insulating state of the latter two can be explained.

(5) The population analyses show that $Sr_2M MoO_6$ have nearly the same valence state combinations due to strong intrinsic $pd$ covalency effects, which accounts for the similar O $2p$-Mo $4d$ spectral structures observed in them.

The author thanks Y. Kakehashi and A. Yaresko for their discussions. This work was cosponsored by Max Planck Society of Germany and National Natural Science Foundation of China.
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In the LSDA+U calculation, the hybridization with the almost full-filled up-spin Cr $t_{2g}$ orbitals induces a finite positive Mo spin, which partly counteracts the large negative Mo spin caused by the down-spin Mo $t_{2g}$ orbitals. The Mo $t_{2g}$ electrons are less itinerant in Sr$_2$CrMoO$_6$ than in SFMO, which is also indicated by comparison of the down-spin Mo $t_{2g}$ bandwidths as seen in Fig. 3.
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Table I. $M$ 3$d$ and $M'$ 4$d$ or 5$d$ population/spin moment (in $\mu_B$) of $A_2$FeReO$_6$ ($A=$Ba,Sr,Ca) and Sr$_2$MMoO$_6$ ($M=$Cr,Mn,Fe,Co) calculated by LSDA and LSDA+$U$.  

|       | LSDA          | LSDA+$U$       |
|-------|---------------|----------------|
|       | $M$           | $M'$           | $M$           | $M'$           |
| $A=$Ba| 5.76/3.72     | 4.46/–0.99     | 5.93/4.16     | 4.50/–1.22     |
| Sr    | 5.62/3.75     | 4.36/–1.05     | 5.87/4.22     | 4.39/–1.27     |
| Ca    | 5.56/3.76     | 4.14/–1.07     | 5.84/4.29     | 4.18/–1.33     |
| $M=$Cr| 3.48/1.67     | 3.34/–0.65     | 3.49/2.42     | 3.40/–0.53     |
| Mn    | 4.62/3.94     | 3.51/–0.17     | 4.81/4.54     | 3.54/0.04      |
| Fe    | 5.65/3.78     | 3.38/–0.44     | 5.89/4.23     | 3.43/–0.60     |
| Co    | 6.85/2.64     | 3.51/–0.20     | 6.96/2.93     | 3.56/–0.12     |
FIGURES

FIG. 1. The LSDA and LSDA+$U$ DOS for the HM FiM state of $A_2\text{FeReO}_6$ ($A$=Ba,Sr,Ca).

The solid (dashed) line denotes the up (down) spin. Fermi level is set at zero.

FIG. 2. Charge density on the (001) plane of $\text{Ba}_2\text{FeReO}_6$, with contour from 0.005 to 0.045 a.u.$^{-3}$ in a step of 0.005 a.u.$^{-3}$ (dashed line), and from 0.05 to 0.5 a.u.$^{-3}$ in a step of 0.05 a.u.$^{-3}$ (solid line). The Re ions are located at center and at corner, and the Fe ions in the middle of edges. The Re and Fe ions are separated by oxygen.

FIG. 3. The LSDA and LSDA+$U$ DOS for the FiM state of $\text{Sr}_2\text{MFeO}_6$ ($M$=Cr,Fe) and for the assumed FM state of $\text{Sr}_2\text{MFeO}_6$ ($M$=Mn,Co).
Fig. 1 Wu

A=Ba

A=Sr

A=Ca

DOS (states/eV)---LSDA

DOS (states/eV)---LSDA+U

ENERGY (eV)

ENERGY (eV)

ENERGY (eV)
Fig2. Wu

Up-Spin Density

Down-Spin Density
Fig. 3 Wu

**M = Cr**

- Total
- Cr $t_{2g}$
- Cr $e_g$
- Mo $t_{2g}$
- Mo $e_g$
- O $2p$

**M = Mn**

- Total
- Mn $t_{2g}$
- Mn $e_g$
- Mo $t_{2g}$
- Mo $e_g$

**M = Fe**

- Total
- Fe $t_{2g}$
- Fe $e_g$
- Mo $t_{2g}$
- Mo $e_g$

**M = Co**

- Total
- Co $t_{2g}$
- Co $e_g$
- Mo $t_{2g}$
- Mo $e_g$
- ab-O $2p$
- c-O $2p$

Energy (eV) vs. DOS (states/eV) for LSDA and LSDA+U calculations.