The dimensional crossover of quantum transport properties in few-layered Bi$_2$Se$_3$ thin films

Liang Yang, Zhenhua Wang, *ab Mingze Li, *b Xuan P. A. Gao c and Zhidong Zhang ab

Topological insulator bismuth selenide (Bi$_2$Se$_3$) thin films with a thickness of 6.0 quintuple layers (QL) to 23 QL are deposited using pulsed laser deposition (PLD). The arithmetical mean deviation of the roughness ($R_a$) of these films is less than 0.5 nm, and the root square mean deviation of the roughness ($R_{sq}$) of these films is less than 0.6 nm. Two-dimensional localization and weak antilocalization are observed in the Bi$_2$Se$_3$ thin films approaching 6.0 nm, and the origin of weak localization should be a 2D electron gas resulting from the split bulk state. Localization introduced by electron–electron interaction (EEI) is revealed by the temperature dependence of the conductivity. The enhanced contribution of three-dimensional EEI and electron–phonon interaction in the electron dephasing process is found by increasing the thickness. Considering the advantage of stoichiometric transfer in PLD, it is believed that the high quality Bi$_2$Se$_3$ thin films might provide more paths for doping and multilayered devices.

Introduction

Topological insulators (TI) are materials with an insulating bulk state (BS) and conducting surface state (SS) which originates from the strong spin–orbit coupling (SOC), and the topological SS is protected by time reversal symmetry (TRS) or lattice symmetries.1–4 The surface band has a linear dispersion relationship near the Dirac point at the high symmetry point.5 Such a SS hosts a massless two dimensional electron gas (2DEG). The most commonly studied three-dimensional (3D) TI with a single Dirac cone and protected by TRS are bismuth telluride (Bi$_2$Te$_3$), antimony telluride (Sb$_2$Te$_3$) and bismuth selenide (Bi$_2$Se$_3$).6,7 The primitive cell of these crystals has five atom layers of A1–B1–A2–B1′–A1′ (where A represents selenium (Se) or telluride (Te), and B represents bismuth (Bi) or antimony (Sb)) stacked along the c axis, defined as one quintuple layer (QL).4 Below a critical thickness for the TIs, the SS opens up a gap at the Dirac point.8 The critical thickness is about 6.0 QL, i.e., about 6 nm for Bi$_2$Se$_3$.9 Magnetic doping or the proximity effect breaks the TRS and opens up a gap at the Dirac point, indicating that it would be possible to use them as on and off switches in spintronics.10 In addition, the Majorana fermions at the interface of the TI and the superconducting materials may be exploited in topological quantum computation.11–13 Because of the theoretical significance and promising applications, the TIs have attracted extensive investigation.

The localization of electrons in 2D materials is a classic issue.14–15 Ordinarily the 2D state is localized, whereas the 2D SS of the TI is weakly antilocalized and protected by TRS.16–20 A magnetic field perpendicular to the surface of the TI breaks the TRS, thus the weak antilocalization (WAL) would be broken, leading to negative magnetococonductance (MC).21,22 If the WAL is broken or in competition with weak localization (WL), then a positive MC or the transition from a negative to a positive MC will arise. The positive MC in TI films may originate from the magnetic doping of SS or the proximity effect between TI and magnetic materials,23,24 from the gap opened up in TI ultrathin films,25–27 from the 2D bulk sub-bands in ultrathin films,28,29 from 2DEG tied to a surface band bending effect or from the disorder induced by nonmagnetic doping.30,31 In the SS of the TI, the spin-momentum locking leads to the destructive interference, and thus the electrons of the SS exhibit WAL, which leads to higher conductivity at lower temperatures.32 However, at low temperatures, the conductivity of the TI films usually decreases with decreasing the temperature. In the diffusive regime, the conductivity is dominated by the competition of WAL and WL because of the electron–electron interaction (EEI).33–35

To obtain a greater transport contribution from the topological SS, it is important to obtain TI thin films with a high crystallization quality. The methods usually used for preparing TI thin films include molecular beam epitaxy (MBE),36–40 chemical vapor deposition,41–44 physical vapor deposition,45–48 pulsed laser deposition (PLD)49–50 and sputtering.51–52 The MBE is the method mainly used to obtain flat and thin TI films for fundamental research, because of its advantages of 2D growth,
single crystal yield and easily controlled doping. However, the non-equilibrium process of PLD allows stoichiometric transfer from the target to the film, which gives the possibility of easier doping in TI films.\(^{61}\) The thickness of previously reported TI films deposited by PLD is mostly more than 15 nm, and the arithmetical mean deviation of the roughness \(R_q\) is mostly larger than 1 nm.\(^{65-68}\) Therefore, in order to observe the dimensional crossover of the physical properties of the TI materials, it is necessary to prepare thinner TI films with high quality. In a recently published paper on depositing TI films using PLD, the root square mean deviation of roughness \(R_q\) was decreased to 0.5–0.7 nm, but there existed more than four steps of QL at the surface.\(^{69}\) It is necessary to use flat thin TI film with a large area as the bottom or middle layer of the hetero-structure in devices for spintronics.\(^{64-67}\) Investigating better preparation conditions using PLD for TI thin films with flat surfaces is a significant area of research.

This paper reports on the characteristics of Bi\(_2\)Se\(_3\) thin films with a thickness of 6.0–23 QL deposited using PLD. The c-oriented and flat characteristics were determined using X-ray diffraction (XRD) and transmission electron microscopy (TEM). The \(R_q\) and \(R_a\) of the films were less than 0.5 nm and 0.6 nm, respectively. The positive MC was observed because of the 2DEG introduced by the quantized 2D BS. The EEI correction in the temperature dependence of conductivity is revealed. As the thickness increases, the predominant characteristic of the MC changes from 2D to 3D, and the contribution of the 3D EEI or electron–phonon interaction (EPI) arises. As a result, the dimensional crossover of the quantum transport properties in few-layered Bi\(_2\)Se\(_3\) thin films was successfully revealed.

**Experimental method**

By changing the deposition time, many samples were prepared using the PLD method. In this research, the focus was on four Bi\(_2\)Se\(_3\) samples with thicknesses of 6.0 QL, 7.0 QL, 9.5 QL and 23 QL on a strontium titanate (SrTiO\(_3\)) (1 1 1) substrate. These thicknesses ranged from the critical thickness of Bi\(_2\)Se\(_3\) (6.0 QL) to the thickness in which the magnetoresistance of the surface state was too weak to be investigated (23 QL). The surface of the SrTiO\(_3\) (1 1 1) was cleaned by plasma before deposition. The substrate was heated to 320 °C under a vacuum greater than 2 × 10\(^{-4}\) Pa, and then the chamber was charged argon (Ar) until a pressure of 50 Pa was achieved. After keeping the temperature and pressure stable for 5 min, the film was deposited at a laser energy of 400 mJ and a frequency of 1 Hz. The deposition rate was about 12 nm min\(^{-1}\). The deposition temperature used was the best temperature obtained from previous experimentation, which was similar to temperatures mentioned in previous reports of depositing Bi\(_2\)Se\(_3\) films using PLD.\(^{66,69}\) After the deposition, the sample was cooled at a rate of 5 °C min\(^{-1}\) in an atmosphere of Ar gas at 300 Pa, which reduced the vaporization of Se at low pressures. The optimal conditions of the method are those given previously. Another Bi\(_2\)Se\(_3\) sample with a thickness of 6.5 nm was prepared for tuning using the back gate voltage \(V_G\). To decrease the carrier density and strengthen the tuning effect, this sample was deposited at 300 °C. As the conditions of the laser device gradually changed, together with the natural consumption of fluorine gas, to keep the deposition rate the same as that of other samples, the deposition atmosphere of the tuned sample was raised to Ar at 55 Pa.

The crystal structure of films was determined using an XRD \(\theta–2\theta\) scan result of (Bruker D8 Advence). The TEM (FEI Tecnai F20) was used for the determination of the structure and interface. The TEM sample for the top view was created by transferring the film to a copper grid. Firstly, poly(-methylmethacrylate) (PMMA) was used to cover the surface of a Bi\(_2\)Se\(_3\) sample by spin coating, and then the sample was heated to 180 °C for the chemicals to fuse. Secondly, a blob of epoxy resin, in which a stick was laid, was used to cover the PMMA layer. After the epoxy resin solidified, the stick divided the combination of Bi\(_2\)Se\(_3\)/PMMA/epoxy resin. Then the combined sample was immersed in acetone to dissolve the PMMA layer. After a few seconds, the Bi\(_2\)Se\(_3\) layer fell into the acetone and was picked up using a copper grid.

The surface pattern of the samples was measured using atomic force microscopy (AFM, Bruker MultiMode8). Because of the van der Waals contact at the interface of the film and substrate, the film could be easily scratched using a toothpick, and then the difference in height, i.e., the thickness of the film, was measured using AFM. When there were 2 QL steps at the surface of the film, the thickness is defined as the average height of the exposed two steps from the substrate. Where there were 3 QL steps at the surface, the thickness is defined as the height of the middle step from the substrate. The roughness of the samples was calculated using NanoScope Analysis software (Bruker). Electrical measurements were made on samples in the shape of a Hall bar with five terminals. The resistivity and Hall resistance of the samples of various thicknesses were measured using a physical property measurement system (PPMS, Quantum Design) with indium (In) as the contacts. The transport properties of the tuned sample were measured using a home-made electrical property measurement system. Silver paint was used as the gate electrode.

**Results and discussion**

The crystal structure of Bi\(_2\)Se\(_3\) is illustrated in Fig. 1(a), and Fig. 1(b) shows the structure viewed from the top, along the c axis. One QL and the covalent bonds between the Bi and Se atoms are shown. Fig. 1(c) shows the high resolution transmission electron microscopy (HRTEM) image for the sectional view of the film with a thickness of 6.0 QL, in which the periodic characteristics are observed. The period is 0.96 nm, equal to the thickness of one QL. Because of the preparation process of the TEM samples with mechanical grinding and heating in the air, the surface and the interface which were in contact with the van der Waals forces were partly damaged, thus they are not very clear in the HRTEM image. The bright field image in the top view is shown in Fig. 1(d). During the transmission of electrons with high energy, the sample warps and cracks at the grain boundaries. Thus, the grains are resolvable because of the diffraction contrasts. Fig. 1(e) is the HRTEM image of the zone in the red frame in Fig. 1(d), which includes three grains, and
the grain boundaries are marked in orange. The axial vectors $a$ and $b$ of the three grains point to different directions. Fig. 1(f) is the enlarged image of the grain marked as 1, and the fast Fourier transform (FFT) image of it is shown in the inset. The interplanar distance of the $(2 2 0)$ planes were measured and found to be 0.21 nm, from which the value of $a$ in this grain was calculated to be 0.42 nm. The TEM results show the high crystallization quality of the sample.

The XRD spectra of the films with different thicknesses are shown in Fig. 2. As shown in Fig. 2(a), all the samples show the $(0 0 3n)$ diffraction peaks of Bi$_2$Se$_3$, indicating a perfect $c$-orientation of the films. The peaks of In are from the incompletely removed In contacts on the sample after electronic measurement. It is worth noting that clear Kiessig fringes were observed in these samples, which revealed the high homogeneity of the films. The first order Kiessig peaks moves closer to the $(0 0 3n)$ main peak with increasing thickness, as indicated by the arrows in Fig. 2(b), which shows the enlarged spectra. The XRD results proved that the samples did have a $c$-oriented Bi$_2$Se$_3$.

The AFM measurements were used for investigating the surface condition of the samples of various thicknesses, and the results are shown in Fig. 3. All the films were continuous. The $R_a$ of all the samples was in the range of 0.27–0.45 nm, and the $R_q$ was in the range of 0.38–0.60 nm. In detail, the height profiles of

---

Fig. 1  (a) The crystal structure of Bi$_2$Se$_3$. (b) The top view of the structure along the $c$-axis. (c) HRTEM image of the Bi$_2$Se$_3$ film with a thickness of 6.0 QL on a SrTiO$_3$ substrate. (d) The bright field TEM image view from the top of the film. (e) The HRTEM image of the zone in the red frame in (d). (f) The enlarged HRTEM image of the grain marked as 1 in (e) and its FFT image.

Fig. 2  (a) XRD results of Bi$_2$Se$_3$ films. The diffraction peak of the substrate is in the range broken on $x$-axis. (b) The enlarged spectra of (a). The arrows indicate the position of the first order Kiessig peak.

Fig. 3  AFM results for the Bi$_2$Se$_3$ samples of (a) 6.0 QL, (b) 7.0 QL, (c) 9.5 QL, and (d) 23 QL. The height profiles of the regions marked by the blue lines are located below the corresponding 2D images.
the areas indicated by the blue lines are included below the corresponding 2D images. All four samples were stacked in layers, and the thickness of each layer was about 1 nm, i.e., 1 QL, as measured in the height profiles. At the surface of the film, the difference of height between the highest step and the lowest step was 2 QL. Namely, the Bi$_2$Se$_3$ films near 6 QL with a flat surface feature prepared using PLD. Such a feature is the same for the Bi$_2$Se$_3$ films deposited using MBE, and this indicated the potential of PLD for depositing TIs and other layered materials. This provided the chance to observe the intrinsic physical properties of TIs near the critical thickness of the dimensional crossover.

The dependence of transport properties on temperature and thickness of the samples in zero magnetic field is shown in Fig. 4. The inset of Fig. 4(a) indicates the sample measurement geometry. The resistivity decreases with decreasing temperature from 300 K, then shows an upturn below the transition temperature. The decrease of resistivity below 300 K is considered as the metallic characteristic of the bulk state, attributed to the lack of Se. The increase of resistivity at low temperatures becomes weaker in thicker samples, indicating the 2D origin of the upturn at low temperatures, as shown in Fig. 4(a). Such a metal-insulator-like transition indicated that the WL was in a diffusive mode or a strong localization was in hopping mode, and this depended on the condition of the sample. The correction of WAL and EEI to the conductivity is given by:

$$\Delta \sigma = \frac{e^2}{2\pi^2\hbar} \left( 1 + \alpha p - \frac{3}{4} F \right) \ln \left( \frac{T}{T_0} \right)$$  \hspace{1cm} (1)

where $\hbar$ is the reduced Planck constant, $\alpha$ is the coefficient in Hikami–Larkin–Nagaoka (HLN) theory, $p$ is the parameter from the temperature dependence of the phase coherence length $l_p \propto T^{-\beta/2}$, $F$ is the screening factor, and $T_0$ is the characteristic temperature at which the EEI effect on the conductivity vanishes. To determine the localization of the samples at low temperatures, the temperature dependences of conductivity in the range of 2–10 K of the Bi$_2$Se$_3$ samples were investigated, and the results are shown in Fig. 4(b). Fig. 4(b) displays the plots of the $G/G_{\text{max}} - \ln T$ relationship, which shows linear behavior. Such a linear behavior signifies that the carriers are in the diffusive regime.

In addition, the carrier density ($n$) and mobility ($\mu$) were calculated and are shown in Fig. 4(c) and (d). The values of $n$ had a negative correlation with thickness, as illustrated in Fig. 4(c) and its inset. This correlation is because of the complicated combination of the carriers from SS and BS or sub-bands of BS. Considering that the Bi : Se ratio of the target is just 2 : 3, the $n$ of the films could be depressed in the future by adding Se or other elements to the target. Fig. 4(d) gives the temperature and thickness dependences of $\mu$. The $\mu$ of thicker films is higher at the same temperature. The inset of Fig. 4(d) illustrates the $\mu$-thickness relationship at 2 K. The value of $\mu$ at 2 K increases from 86 cm$^2$ V$^{-1}$ s$^{-1}$ to 531 cm$^2$ V$^{-1}$ s$^{-1}$ as the thickness increases from 6.0 QL to 23 QL. This increase can be attributed to the disappearance of cavities and better crystallization because of the lengthening of the deposition time. The mobility of the samples exceeds the value of most of the Bi$_2$Se$_3$ and Bi$_3$Te$_3$ films deposited using PLD, which indicated improved crystal quality.

The magneto-transport property [$\Delta G = G (H) - G (0)$] of the four samples was measured in the range of $-7 \text{T}$ to $7 \text{T}$, and the results are shown in Fig. 5. Obvious cusps were obtained in thinner films near a magnetic field of zero. The cusp was weaker with increasing film thickness or temperature, indicating that

Fig. 4  (a) $\rho$–$T$ relationship of Bi$_2$Se$_3$ samples of various thicknesses. The inset indicates the sample measurement geometry. (b) The temperature dependences of $G/G_{\text{max}}$ plotted against $\ln T$. The temperature scale used is $2$–$10 \text{K}$. The dashed lines are a guide for the eye. (c) The relationship between $n$ and $T$ of the samples of various thicknesses; the inset is the change of $n$ with samples of different thicknesses at $2 \text{K}$. (d) The temperature and thickness dependences of $\mu$; the inset is the thickness dependence of $\mu$ at $2 \text{K}$.

Fig. 5  The MC of the Bi$_2$Se$_3$ samples with thicknesses of (a) 6.0 QL, (b) 7.0 QL, (c) 9.5 QL and (d) 23 QL in a perpendicular magnetic field.
the WAL was the origin. In the films with thicknesses of 6.0 QL or 7.0 QL, a positive MC appeared in the high magnetic field range, and was weakened as the thickness increased. Such a phenomenon was also discovered and investigated in Bi$_2$Se$_3$ films deposited using MBE, and was explained by the WL of the quantized BS.\textsuperscript{29} In the 9.5 QL and 23 QL films, the parabolic characteristic in a high magnetic field range became increasingly obvious with the increasing thickness, for which the MC of BS was responsible.

The origin of the positive MC was explored by measuring the conductance of four samples in a magnetic field with different directions at 2 K. Fig. 6(a) shows the MC in the perpendicular magnetic field ($H_\parallel$). As the thickness increased, the high-field positive MC characteristic disappeared, and the parabolic characteristic emerged. Fig. 6(b) illustrates the MC in the parallel magnetic field ($H_\perp$). In $H_\parallel$, the negative MC increased as the thickness increased, and a positive MC did not appear. Therefore, it was deduced that the positive MC was an effect in $H_\perp$ and was possibly attributed to the 2DEG from the 2D subbands of the quantized BS.\textsuperscript{28–31}

As a TI, the transport of the SS of Bi$_2$Se$_3$ films was analyzed. According to HLN theory, the situation with a strong SOC and no magnetic scattering, the magnetoconductivity in a low field is determined using a simplified equation:\textsuperscript{35,21,82}

$$\Delta \sigma(B) = -\alpha \frac{e^2}{2\pi^2h} \left[ \psi \left( \frac{1}{2} + \frac{B_0}{B} \right) - \ln \left( \frac{B_0}{B} \right) \right]$$

where $h$ is the reduced Planck constant, $\psi$ is the digamma function, $B_0 = h/(4D\epsilon_{\alpha}) = h/(4el_0^2)$ is the characteristic field, $l_\phi$ is the phase coherence length, $D$ is the diffusion constant. For the 2D SS of 3D TI with a single Dirac cone, parameter $\alpha = 0.5$. By fitting the MC data below 0.1 T to HLN theory, $\alpha$, $l_\phi$, and $p$ of these samples with various thicknesses was obtained, as shown in Fig. 7. The WAL characteristic of the sample with a thickness of 23 QL was too weak to fit, thus those data were not included. As shown in Fig. 7(a) and its inset, the values of $\alpha$ in all the samples at 2 K were smaller than 0.6, and were not monotonically correlated with thickness. There were two SS in one sample, so the theoretical $\alpha$ was 1 for TI films with one Dirac cone. The value of $\alpha$ less than 1 was interpreted using the coupling of SS and BS in the thick film samples or the coupling of top and bottom SS for the thin samples.\textsuperscript{83–85} The value of $\alpha$ increased with decreasing temperature, which indicated the decoupling tendency. The value of $l_\phi$ was in the range of 206–881 nm in the samples at 2 K, and it increased as the thickness increased, suggesting that the grain boundaries and defects diminished with longer deposition time. Thus, the quality of the sample could be further improved by annealing under a capped layer or in a Se atmosphere. The values of $l_\phi$ at 2 K were larger, by one order of magnitude, than that of the reported Bi$_2$Se$_3$ films prepared using PLD,\textsuperscript{34,55,86} but were comparable with that of Bi$_2$Se$_3$ films with the same thickness prepared using MBE and van der Waals epitaxy.\textsuperscript{45,87} A long $l_\phi$ signified weak inelastic scattering, which indicated the high quality of the films.\textsuperscript{88}

The perfect linear dependence of logarithmic $l_\phi$ on $\ln T$ is shown in Fig. 7(b), which signified the relationship of $l_\phi \propto T^{-\pi/2}$. By fitting the data, a monotonically increasing tendency of $p$ with increasing the thickness was obtained, as plotted in the inset of Fig. 7(b). The value of $p$ increased from about 0.91 to near 1.56. The theoretical values of $p$ were 1, 1.5 and 3 corresponding to the dephasing mechanism of 2D EEI, 3D EEI and EPI, respectively.\textsuperscript{14,77,89} Thus, the tendency of $p$ to increase indicated the enhanced contribution of 3D EEI or EPI in the dephasing process.

To further investigate the transport properties of Bi$_2$Se$_3$ samples deposited using PLD and identify the coupling mechanism, the sample deposited at 300 °C was tuned using a back gate. The $R_s$ and $R_q$ of the sample were 0.30 nm and 0.44 nm, respectively, as shown by the AFM image in the inset of Fig. 8(a). The $p$–$T$ curve of this sample in Fig. 8(a) presents a metallic behaviour at high temperatures and a metal-insulator like transition at about 20 K. The values of $\alpha$ and $\mu$ under various $V_G$ are calculated and shown in Fig. 8(b). The value of $\alpha$ with $V_G = 0$ V was about $2.6 \times 10^{19}$ cm$^{-3}$, lower than that of the samples deposited at 320 °C. This demonstrates that the decreased deposition temperature and increased Ar pressure reduce the amount of Se in the film. For a range of $V_G$ from 0 V to −190 V, $n$ decreased from $2.6 \times 10^{19}$ cm$^{-3}$ to $1.4 \times 10^{18}$ cm$^{-3}$, i.e., the sheet carrier density decreased from $1.5 \times 10^{13}$ cm$^{-2}$ to 0.9 $\times 10^{13}$ cm$^{-2}$, signifying that the Fermi surface was tuned to the bulk condition band edge.\textsuperscript{85} The value of $\mu$ with $V_G = 0$ V was 57 cm$^2$ V$^{-1}$ s$^{-1}$, lower by almost half than that for the samples deposited at 320 °C with a similar thickness. This can be
attributed to the presence of more cavities and worse crystallization with decreased deposition temperature. The value of $\mu$ has a negative correlation with $V_{G}$, depending on the band structure near the Fermi surface.

Tuning the MC of the film using $V_{G}$ gives a reasonable interpretation of the $\alpha$ which were less than 1. As shown in Fig. 8(c), the MC curves in $H_{\perp}$ have a $V_{G}$ dependence. The MC curves show the WAL characteristic in the low magnetic field, and the WL behaviour of positive MC appeared in the high magnetic field range, which was similar to the samples deposited at 320 °C. When the $V_{G}$ was decreased, the width of the cusp in the low $H_{\perp}$ became larger, and this agreed with the results found in previous investigations. As shown in Fig. 8(d), as $V_{G}$ decreased from 0 V to −190 V, $\alpha$ decreased from about 0.51 to 0.31, whereas the change of $l_{p}$ was smaller than 10% and fluctuated. Therefore, the larger width of the cusp in low $H_{\perp}$ was mainly because of the decreased $\alpha$. In the n-type Bi$_2$Se$_3$ films, a negative $V_{G}$ caused the SS and BS to decouple, resulting in the increased $\alpha$ as the $V_{G}$ decreased. However, this is the opposite of the $\alpha$-$V_{G}$ relationship found in this research, which means that the coupling of two SS is the primary mechanism of the $\alpha$ less than 1 in such a thin sample. The tuning of the thick samples need more negative $V_{G}$, which was beyond the ability of the equipment used in this research. For films thick enough to avoid the hybridization of two SS, the primary mechanism may be the coupling of SS and BS.

**Conclusions**

Bi$_2$Se$_3$ thin films with a (0 0 1) orientation with thicknesses of 6.0–23 QL are prepared using PLD, and their properties were systematically investigated. The $R_{in}$ and $R_{q}$ of the films were smaller than 0.5 nm and 0.6 nm, respectively. Steps of QL were observed at the surfaces of all the samples. In the films near the critical thickness, the transition from WAL to WL characteristic appears upon increasing the magnetic field and the WL characteristic disappears upon increasing the thickness. By investigating MC with different directions of magnetic fields, it was determined that the WL characteristic was a 2D effect in $H_{\perp}$, which was possibly attributed to 2DEG from the 2D subbands of BS. It was found that the value of $\alpha$ was less than 0.6, which demonstrated the coupling of two SS for thin samples and the possible coupling of SS and BS for thick samples. In addition, the value of $l_{p}$ showed a negative logarithmic dependence on temperature, and increased with increasing thickness. Furthermore, as the thickness increased, the mechanism of the dephasing process gradually changed from simply 2D EEI to including increased 3D EEI or EPI. The observation of dimensional crossover for the quantum transport properties of Bi$_2$Se$_3$ thin films indicated that the PLD was a powerful method for preparing TI thin films of high quality, which is very important for further applications.

**Conflicts of interest**

There are no conflicts to declare.

**Acknowledgements**

This research was supported by the National Natural Science Foundation of China (Grant Nos 51522104, 51331006) and the National Basic Research Program (No. 2017YFA0206302). XPAG thanks the National Science Foundation (DMR-1151534) for financial support.

**References**

1. L. Fu, *Phys. Rev. Lett.*, 2011, **106**, 106802.
2. G. A. Fiete, *Nat. Mater.*, 2012, **11**, 1003.
3. L. Fu and C. Kane, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2007, **76**, 045302.
4. H. Zhang, C.-X. Liu, X.-L. Qi, X. Dai, Z. Fang and S.-C. Zhang, *Nat. Phys.*, 2009, **5**, 438–442.
5. M. Z. Hasan and C. L. Kane, *Rev. Mod. Phys.*, 2010, **82**, 3045–3067.
6. X.-L. Qi and S.-C. Zhang, *Rev. Mod. Phys.*, 2011, **83**, 1057–1110.
7. B. Yan and S.-C. Zhang, *Rep. Prog. Phys.*, 2012, **75**, 096501.
8. K. Nakayama, K. Eto, Y. Tanaka, T. Sato, S. Souma, T. Takahashi, K. Segawa and Y. Ando, *Phys. Rev. Lett.*, 2012, **109**, 236804.
9. K. He, Y. Zhang, K. He, C.-Z. Chang, C.-L. Song, L.-L. Wang, X. Chen, J.-F. Jia, Z. Fang, X. Dai, W.-Y. Shan, S.-Q. Shen, Q. Niu, X.-L. Qi, S.-C. Zhang, X.-C. Ma and Q.-K. Xue, *Nat. Phys.*, 2010, **6**, 584–588.
10. C.-Z. Chang, P. Wei and J. S. Moodera, *MRS Bull.*, 2014, **39**, 867–872.
11. P. Zareapour, A. Hayat, S. Y. F. Zhao, M. Kreshchuk, A. Jain, D. C. Kwok, N. Lee, S.-W. Cheong, Z. Xu, A. Yang, G. D. Gu,
56. A. M. Adam, E. Lilov, V. Lilova and P. Petkov, *Mater. Sci. Semicond. Process.*, 2017, 57, 210–219.
57. L. Meng, H. Meng, W. Gong, W. Liu and Z. Zhang, *Thin Solid Films*, 2011, 519, 762–7631.
58. R. Zeipl, M. Jelinek, M. Vlcek, T. Kocourek, J. Remsa and J. Vanis, *Laser Phys.*, 2015, 25, 015903.
59. P. Chaturvedi, D. Saha and S. Ganguly, *AIP Conf. Proc.*, 2016, 1731, 080056.
60. C. Bigi, P. Orgiani, A. Nardi, A. Trogla, J. Fujii, G. Panaccione, I. Vobornik and G. Rossi, *Appl. Surf. Sci.*, 2019, 473, 190–193.
61. P. Sahu, J.-Y. Chen, J. C. Myers and J.-P. Wang, *Appl. Phys. Lett.*, 2018, 112, 122402.
62. W. J. Wang, K. H. Gao and Z. Q. Li, *Sci. Rep.*, 2016, 6, 25291.
63. R. Eason, *Pulsed Laser Deposition of Thin Films*, John Wiley & Sons, Inc., Hoboken, New Jersey, USA, 2007, p. 28.
64. Y. Wang, D. Zhu, Y. Wu, Y. Yang, J. Yu, R. Ramaswamy, R. Mishra, S. Shi, M. Elyasi, K. L. Teo, Y. Wu and H. Yang, *Nat. Commun.*, 2017, 8, 1364.
65. P. P. Shibayev, E. J. Konig, M. Salehi, J. Moon, M. G. Han and S. Oh, *Nano Lett.*, 2019, 19, 716–721.
66. Y. Hou and R. Wu, *Nano Lett.*, 2019, 19, 2472–2477.
67. S. Cha, M. Noh, J. Kim, J. Son, H. Bae, D. Lee, H. Kim, J. Lee, H. S. Shin, S. Sim, S. Yang, S. Lee, W. Shim, C. H. Lee, M. H. Jo, J. S. Kim and H. Choi, *Nat. Nanotechnol.*, 2018, 13, 910–914.
68. S. X. Zhang, L. Yan, J. Qi, M. Zhuo, Y. Q. Wang, R. P. Prasankumar, Q. X. Jia and S. T. Picraux, *Thin Solid Films*, 2012, 520, 6459–6462.
69. P. H. Le, K. H. Wu, C. W. Luo and J. Leu, *Thin Solid Films*, 2013, 534, 659–663.
70. S. Schreyeck, N. V. Tarakina, G. Karczewski, C. Schumacher, T. Borzenko, C. Brüne, H. Buhmann, C. Gould, K. Brunner and L. W. Molenkamp, *Appl. Phys. Lett.*, 2013, 102, 041914.
71. J. M. Hartmann, A. Abbadie and S. Favier, *J. Appl. Phys.*, 2011, 110, 083529.
72. X. Leng, J. Pereiro, J. Strle, G. Dubuis, A. T. Bollinger, A. Gozar, J. Wu, N. Litombe, C. Panagopoulos, D. Pavuna and I. Božović, *npj Quantum Mater.*, 2017, 2, 35.
73. M. Wang, S. Shen, J. Ni, N. Lu, Z. Li, H. B. Li, S. Yang, T. Chen, J. Guo, Y. Wang, H. Xiang and P. Yu, *Adv. Mater.*, 2017, 29, 1703628.
74. M. Liu, C.-Z. Chang, Z. Zhang, Y. Zhang, W. Ruan, K. He, L.-l. Wang, X. Chen, J.-F. Jia, S.-C. Zhang, Q.-K. Xue, X. Ma and Y. Wang, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2011, 83, 165440.
75. Y. S. Hor, J. G. Checkelsky, D. Qu, N. P. Ong and R. J. Cava, *J. Phys. Chem. Solids.*, 2011, 72, 572–576.
76. P. Shang, X. Guo, B. Zhao, X. Dai, L. Bin, J. Jia, Q. Li and M. Xie, *Nanotechnology*, 2016, 27, 085601.
77. P. A. Lee and T. V. Ramakrishnan, *Rev. Mod. Phys.*, 1985, 57, 287–337.
78. J. Liao, Y. Ou, X. Feng, S. Yang, C. Lin, W. Yang, K. Wu, K. He, X. Ma, Q. K. Xue and Y. Li, *Phys. Rev. Lett.*, 2015, 114, 216601.
79. P. A. Lee and D. S. Fisher, *Phys. Rev. Lett.*, 1981, 47, 882–885.
80. Y. F. Lee, S. Punugupati, F. Wu, Z. Jin, J. Narayan and J. Schwartz, *Curr. Opin. Solid State Mater. Sci.*, 2014, 18, 279–285.
81. P. H. Le, C.-N. Liao, C. W. Luo, J.-Y. Lin and J. Leu, *Appl. Surf. Sci.*, 2013, 285,[Part B], 657–663.
82. P. E. J. König, P. M. Ostrovsky, I. V. Protopopov, I. V. Gornyi, I. S. Burmistrov and A. D. Mirlin, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2013, 88, 035106.
83. H. Steinberg, J. B. Laloë, V. Fatemi, J. S. Moodera and P. Jarillo-Herrero, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2011, 84, 233101.
84. I. Garate and L. Glazman, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2012, 86, 035422.
85. D. Kim, P. Syers, N. P. Butch, J. Paglione and M. S. Fuhrer, *Nat. Commun.*, 2013, 4, 2040.
86. P. H. Le, S.-P. Chiu, S.-R. Jian, C. W. Luo, J.-Y. Lin, J.-J. Lin, K. H. Wu and M. Gospodinov, *J. Alloys Compd.*, 2016, 679, 350–357.
87. N. Bansal, Y. S. Kim, M. Brahlek, E. Edrey and S. Oh, *Phys. Rev. Lett.*, 2012, 109, 116804.
88. A. A. Taskin, S. Sasaki, K. Segawa and Y. Ando, *Adv. Mater.*, 2012, 24, 5581–5585.
89. H.-C. Liu, H.-Z. Lu, H.-T. He, B. Li, S.-G. Liu, Q. L. He, G. Wang, I. K. Sou, S.-Q. Shen and J. Wang, *ACS Nano*, 2014, 8, 9616–9621.
90. J. Chen, H. J. Qin, F. Yang, J. Liu, T. Guan, F. M. Qu, G. H. Zhang, J. R. Shi, X. C. Xie, C. L. Yang, K. H. Wu, Y. Q. Li and L. Lu, *Phys. Rev. Lett.*, 2010, 105, 176602.