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Why Do the Maximum Intensities in Modeled Tropical Cyclones Vary Under the Same Environmental Conditions?

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Abstract In this study we explored why the different initial tropical cyclone structures can result in different steady-state maximum intensities in model simulations with the same environmental conditions. We discovered a linear relationship between the radius of maximum wind (r_m) and the absolute angular momentum that passes through r_m (M_m) in the model simulated steady-state tropical cyclones that r_m = aM_m + b. This nonnegligible intercept b is found to be the key to making a steady-state storm with a larger M_m more intense. The sensitivity experiments show that this nonzero b results mainly from horizontal turbulent mixing and decreases with decreased horizontal mixing. Using this linear relationship from the simulations, it is also found that the degree of supergradient wind is a function of M_m as well as the turbulent mixing length such that both a larger M_m and/or a reduced turbulent mixing length result in larger supergradient winds.

Plain Language Summary According to the maximum potential intensity theory, the maximum intensities for tropical cyclones should be the same given the same environmental conditions, which means the radius of maximum wind (r_m) at the boundary layer top should be linearly proportional to the absolute angular momentum such that r_m = aM_m. In model simulations, however, different initial vortex structures usually result in different quasi-steady-state maximum intensities. In this paper, an axisymmetric numerical model is used to evaluate the TC's maximum intensities at the quasi-steady state and explore the cause of this discrepancy between the model simulations and the maximum potential intensity theory. The model results exhibit that the various values of r_m do have a linear relation with M_m, which is predicted by the maximum potential intensity theory. However, there is a non-negligible intercept term, b, in this linear relation (r_m = aM_m + b), which is found to be the key to making a steady-state storm with a larger M_m more intense.

1. Introduction

The size and intensity of tropical cyclones (TCs) as well as their relationship have been explored by many modeling and observational studies. Merrill (1984) found that the radius of outermost closed isobar is weakly correlated to a TC’s intensity. Meanwhile, the statistical analysis shows that the intensification rate has a weak negative correlation with the radius of maximum wind and the radius of gale-force wind (Carrasco et al., 2014; Xu & Wang, 2015). It is also found through idealized model simulations that the size of a mature TC is highly dependent on its initial vortex (Chan & Chan, 2014; Xu & Wang, 2010). However, the relationship between the TC size and intensity is still unclear due to the complexity of external and internal factors that contribute to their evolution. In order to systematically evaluate the relationship between intensity and size, a more quantitative analysis based on theoretical TC dynamics is needed. Since theoretical work has been well established for steady-state TCs, it is beneficial to first investigate the relationship between the size and intensity of steady-state TCs.

Tropical cyclones theoretically have one maximum potential intensity (MPI; see the supporting information for MPI’s two interpretations) in a given environment, which is mainly determined by the environmental parameters (Emanuel, 1986, 1988, 1995; Emanuel & Rotunno, 2011, hereinafter ER11; Shutts, 1981). This environmental control would indicate that the tropical cyclone initial conditions and its internal processes would have little influence on the maximum achievable intensity if the tropical cyclone could develop in the same environment without interruption. This environmental limit on maximum achievable TC...
intensity can be understood from the consideration of several factors. The maximum achievable intensity is the intensity that can balance the mechanical energy available from the enthalpy input from the ocean through the surface sensible and latent heat fluxes and its dissipation in the boundary layer (Emanuel, 1997). The structure of the TC above the boundary layer is such that the angular momentum surfaces emerging from the boundary layer cannot penetrate the tropopause. This puts a strong constraint on the radial location of the angular momentum surface that passes through the radius of maximum wind, and hence the maximum achievable intensity.

The MPI under the foregoing considerations will be the same for the same environment (detailed derivations are shown in the supporting information). Given that the Coriolis term is much smaller than the tangential wind term at the radius of maximum wind in the expression of absolute angular momentum, we have \( M_m = r_m V_m + \frac{1}{2} r_m^2 \sigma M_m \), where \( r_m \) is the radius of maximum wind, \( V_m \) is the maximum tangential wind, \( M_m \) is the angular momentum surface that passes through \( r_m \). Since the value of \( V_m \) is the same for steady-state storms in the same environment, according to the MPI theories, all of the variation in \( M_m \) should be that of \( r_m \) and there should exist a linear relationship between \( M_m \) and \( r_m \) that depends only on environmental conditions. In seeming contradiction of the foregoing theoretical results, the final quasi-steady-state maximum intensities of different initial vortices in the same environment in model simulations are usually significantly different from each other (Rotunno and Emanuel, 1986; Xu & Wang, 2010, 2018). We attempt here to at least partially address this phenomenon in simulated TCs and find the relation among \( V_m, r_m \), and \( M_m \). Section 2 describes the model simulation setup. Section 3 presents the results from the simulations. Summary is provided in section 4. At the end of the paper, we will also discuss the application of this study to better understanding TC intensity and size, and explain the new insights in the forecasting of future TCs.

### 2. Model Setups

We use the axisymmetric version of the nonhydrostatic Cloud Model, version 1 (CM1), as described in Bryan and Rotunno (2009). The domain is 1,500 km in radius with a grid spacing of 1 km for \( r < 300 \) km and linearly stretched to 15 km for \( r \geq 300 \) km. There are 140 vertical levels, with the lowest model level at 25 m above the surface and the highest model level at 25 km. The vertical grid spacing varies from 50 to 200 m for \( z < 5 \) km and is fixed to 200 m for \( z \geq 5 \) km. A constant Coriolis parameter (\( f = 5 \times 10^{-5} \text{ s}^{-1} \)) and a constant sea surface temperature (28 °C) are used. The vertical turbulent mixing length is set to 100 m, while the horizontal turbulent mixing length is set to 1,000 m. There are three sets of experiments with a fixed \( C_k = 10^{-3} \) but varying \( C_d \) to obtain \( \frac{C_k}{C_d} = 0.5, 1.0, 1.5 \), respectively (CkCd0.5, CkCd1.0, CkCd1.5). Two extra sensitivity sets with smaller horizontal turbulent mixing lengths (100 and 500 m, respectively; CkCd1.0_lh100, CkCd1.0_lh500) are performed to explore the role of horizontal turbulent mixing in modulating the relation among steady-state \( M_m, r_m \), and \( V_m \).

The radial profiles of the initial surface tangential winds using equation (1) of Xu and Wang (2018) are shown in Figure 1. The initial maximum surface wind is 20 m s\(^{-1}\) for all simulations. There are 5 different initial \( r_m \) values (\( r_m = 60, 75, 90, 105, \) and 120 km, respectively) and two different “skirt” parameters (\( B = 1.0 \) and 0.75, respectively; a smaller \( B \) produces a broader radial profile). The tangential wind vanishes at \( r = 1,500 \) km. The simulation times are 192 hr for CkCd1.0 and 240 hr for CkCd0.5 and CkCd1.5, which are enough for \( r_m \) and \( V_m \) to reach a quasi-steady state under current environmental and model setups.

### 3. Results

The simulation results for the maximum tangential wind at the boundary layer top (\( z = 1.55 \) km) are shown in the first row of Figure 2. As presented in previous studies (ER11; Bryan, 2012; Peng et al., 2018), a larger \( \frac{C_k}{C_d} \) ratio tends to generate a larger final maximum intensity. In addition, we find that for the simulations with the same \( B \) within the same \( \frac{C_k}{C_d} \) set, the larger the initial \( r_m \) is, the larger the maximum intensity is. At the same

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**Figure 1.** Initial surface tangential wind profiles: a larger \( B \) indicates a \( V(r) \) that decays faster outside of \( r_m \). The profiles are from equation (1) of Xu and Wang (2018).
time, the smaller B values (broader initial radial profile) result in larger final maximum intensities for the same initial \( r_m \) and the same \( \frac{C_k}{C_d} \). The final \( r_m \) (second row of Figure 2) is less sensitive to \( \frac{C_k}{C_d} \) but quite different among different initial vortex profiles that the values of \( r_m \) will keep their ranking order during development, which is consistent with Xu and Wang (2010). While it is not the focus of this study, we also note that the smaller vortices intensify more quickly and reach their final values of \( r_m \) sooner than the larger vortices. It is also worth mentioning that given the same initial vortex, the storm takes more time to intensify with a smaller \( C_d \) (Bryan, 2013).

According to the MPI theories, we should expect the same maximum intensity for the same \( \frac{C_k}{C_d} \) and a linear relationship between \( r_m \) and \( M_m \). However, as the first row of Figure 2 shows, the final quasi-steady-state maximum intensities in these simulations under the same environment are significantly different from each other given the different initial storm structures. Generally speaking, in these model simulations, a larger initial vortex will lead to a larger and more intense final vortex given the same environmental conditions.

To further identify the relation among \( V_m, r_m, \) and \( M_m \), we plotted \( r_m \) as a function of \( M_m \) using the values from averaging the last 24 hr of simulation results. Although the same maximum intensity is not observed in Figure 2, linear relationships are found in the model simulations despite the same environmental conditions (first row of Figure 3). We find that

\[
r_m = aM_m + b, \tag{1}
\]

where \( a \) is the slope and \( b \) is the \( r_m \) intercept, both of which are from the linear regression of the data from the simulated steady-state TCs. The values of \( a \) and \( b \) vary with \( \frac{C_k}{C_d} \) (Table 1). The \( a \) value decreases with increasing \( \frac{C_k}{C_d} \), which is partially consistent with the expected trend from the MPI theories since \( V_m \sim \frac{a}{\beta} \) in theory. Meanwhile, there is a nonnegligible \( r_m \) intercept \( b \) in this linear relationship, which is not expected from the MPI theories. In fact, this \( b \) is essential to the variation in \( V_m \). It is worth to clarify that this \( b \) is not from the Coriolis term in the \( M_m \) expression, which is small enough to be neglected at \( r_m \). Using the definition of \( M_m \), we can use the linear relationship (1) to obtain
\[ V_m \approx M_m / (a M_m + b) \] (2)

The second row of Figure 3 exhibits a good agreement between (2) (dash line) and the model results (dots). The nonzero intercept parameter \( b \) in the linear relationship is indicative of the importance of processes not directly considered in the MPI theory. It is known that the MPI theory assumes an inviscid troposphere above the boundary layer as well as balanced dynamics, which are not satisfied in full-physics model simulations. Here we hypothesize that the discrepancy between analytic theory and the modeling results is mainly due to the neglected horizontal turbulent mixing in the derivation of the analytic solutions.

Rotunno and Bryan (2012) found that the horizontal mixing length \( (l_h) \) can influence the maximum simulated intensity and radius of maximum wind significantly through redistributing the angular momentum in the inner core region. Zhang and Marks (2015) also found a positive correlation between the radius of maximum wind and the horizontal mixing rate. It is suggested here that \( a \) and \( b \) could be altered by different horizontal turbulent mixing, which turns out to be the case as shown in Figure 4. The two sensitivity sets (CkCd1.0_lh100 and CkCd1.0_lh500) with smaller horizontal turbulent mixing lengths present that the linear relationship still holds well but with much smaller \( b \), and that \( b \) decreases as \( l_h \) decreases. The slope parameter \( a \) also decreases with smaller \( l_h \), however, the change is less than that in the intercept parameter \( b \). At the same time, the set of CkCd1.0_lh100 generates the highest maximum intensities among CkCd1.0_lh100, CkCd1.0_lh500 and CkCd1.0 not only due to the smaller \( a \) and \( b \) values (Table 1) but also due to achieving the smallest \( r_m \) that \( M_m \) can reach with the reduced horizontal turbulent mixing (Figures 3b, 4c, and 4d).

Another application of the linear relationship in equation (1) is to estimate the intensity greater than that given by the MPI theories. The magnitudes of \( V_m \) from the present CM1 simulations are much larger than

| Table 1 | List of \( a \) and \( b \) values in all sets. |
|---------|--------------------------------------|
|         | CkCd0.5 | CkCd1.0 | CkCd1.5 | CkCd1.0_lh100 | CkCd1.0_lh500 |
| \( a \) [10^{-6} \text{ km} \cdot \text{s/m}^2] | 7.67    | 7.39    | 7.08    | 6.44         | 6.63         |
| \( b \) [km]     | 6.91    | 6.60    | 6.52    | 2.73         | 5.97         |
the MPI especially in the smaller turbulent mixing length experiments. Given that the theoretical maximum intensity from balanced assumptions is independent of storm related parameters, we have

\[ r_m \cong a_0 M_m; \]  

(3)

where \( a_0(=1/V_m0) \) and \( r_m0 \) are the slope and radius of maximum wind from the MPI theories. We use a similar super intensity (SI) index as defined in Rousseau-Rizzi and Emanuel (2019) as

\[ SI = \frac{V_m - V_m0}{V_m0} = \frac{M_m}{aM_m + bM_m} = \frac{a_0}{a + \frac{b}{M_m}} - 1, \]  

(4)

where \( V_m0 \) is the MPI, \( V_m \) is the quasi-steady-state maximum tangential wind of a model simulation. The relation shown in equation (4) suggests that a TC with a larger \( M_m \) has more SI given the same environment (the same \( a_0, a, \) and \( b \)). This SI index is also a good indicator for the magnitude of supergradient winds. Given the same environment, the SI trend from equation (4) is consistent with the degree of gradient wind imbalance (GIB) estimated in Miyamoto et al. (2014) that a TC with a larger \( r_m \) will have larger GIB. At the same time, with less turbulent mixing (smaller \( a \) and \( b \)), the value of SI is larger and the wind field will become more supergradient as shown in Bryan (2012). From another perspective, equation (4) allows the comparison of the SI for different model setups and environmental factors through the comparison of the corresponding \( a_0, a, \) and \( b \).

Figure 4. (a and b) Time evolution of the maximum tangential winds at \( z = 1.55 \) km for CkCd1.0_lh100 and CkCd1.0_lh500. (c-f) The same as Figure 3 but for CkCd1.0_lh100 and CkCd1.0_lh500.
4. Summary and Discussion

This study seeks to know the relations among $M_m$, $r_m$ and $V_m$ in the model simulations of TCs under the same environmental conditions, and what causes the discrepancy between the MPI theories and model simulations. Although the relationship between the TC size and intensity has been explored by some studies (Merrill, 1984; Xu & Wang, 2010), the complex external and internal factors conceal the relationship between them. In the present paper, we find through the analysis of suite of idealized numerical simulations that at the steady state the radius of maximum wind ($r_m$) above the boundary layer top has a linear relationship ($r_m = aM_m + b$) with the absolute angular momentum $M_m$ that passes through $r_m$. The nonnegligible $r_m$ intercept $b$ provides a way to understand why storms with larger $M_m$ and larger $r_m$ are more intense at the steady state in model simulations. The balanced axisymmetric theories for steady-state tropical cyclone predict a linear relationship where $a$ would be based on differing environmental conditions, but a nonzero $r_m$ intercept $b$ is not expected from those theories. It is found here that the horizontal turbulent mixing is responsible for the existence of this nonzero $b$, and that $a$ can depend on turbulent mixing as well as environmental conditions and $C_k/C_d$. The role of horizontal turbulent mixing on modulating the final maximum intensities is through adjusting the linear relationship between $r_m$ and $M_m$ and that less horizontal turbulent mixing will produce both smaller slope $a$ (greater $V_m$) and intercept $b$. Though only the sensitivities of $C_k$ and horizontal turbulent mixing length are tested here, additional tests with varying sea surface temperature and microphysics (not shown) confirm similar linear relationships and we expect the results to hold under different specified environmental and model setups. This linear relationship shows that the processes not included in the balanced axisymmetric TC theories do not completely contaminate the theoretical results but rather modify the relationship. Furthermore, this finding also provides a way to quantify the ratio of the supergradient wind attributed to the processes not included in the classic MPI theory.

The results shown in section 3 can have important practical applications in modeling and forecasting. We have found in the present study the characteristics of the simulated maximum intensity and the radius of maximum wind for quasi-steady-state tropical cyclones under a given environment. Thus, if we can relate the final state to the storm's initial state, we will be able to predict some of the important storm parameters.
to some extent. Figure 5 shows that although $M_m$ is not conserved during development (first row of Figure 5), a larger initial $M_m$ tends to have a larger final $M_m$ (second row of Figure 5). This positive correlation between the initial $M_m$ and final $M_m$ tells us that the final storm structure and intensity have some memory of the initial vortex structure and intensity. Another interesting finding from Figure 5 is that the storms with the smaller initial $M_m$ tends to keep its $M_m$ closer to its original value compared to the larger initial $M_m$ storms. We believe this to be partially related to the fact that storms with larger initial $M_m$ need a longer time to reach a quasi-steady-state (first row of Figure 2), which then increases the possibility of environmental influence during its development stage.

It is also shown in the second row of Figure 5 that the parameter B (controlling the skirt outside $r_m$) has an effect on the final $M_m$; given the same initial $r_m$, the storms with a smaller B value (broader vortex), will have a larger final $M_m$ compared to the storms with a larger B value. However, the B parameter can be changed by the environmental influence during the storm’s early development stage, that is, the modification of sea surface temperature (Sun et al., 2017) and environmental moisture (Hill & Lackmann, 2009) on the moist convections in the rainbands and hence the storm wind structure outside $r_m$. Further exploration of the relationships between initial and final vortex structure in a variety of environmental conditions is warranted and will be the subject of future research.

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