Tracing the Magnetic Field Topology of the Quiet Corona Using Propagating Disturbances

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Abstract

The motion of faint propagating disturbances (PDs) in the solar corona reveals an intricate structure that must be defined by the magnetic field. Applied to quiet Sun observations by the Atmospheric Imaging Assembly (AIA)/Solar Dynamics Observatory (SDO), a novel method reveals a cellular network, with cells of typical diameters 50" in the cool 304 Å channel and 100" in the coronal 193 Å channel. The 193 Å cells can overlie several 304 Å cells, although both channels share common source and sink regions. The sources are points, or narrow corridors, of divergence that occupy the centers of cells. They are significantly aligned with photospheric network features and enhanced magnetic elements. This shows that the bright network is important to the production of PDs and confirms that the network is host to the source footpoint of quiet coronal loops. The other footpoint, or the sinks of the PDs, form the boundaries of the coronal cells. These are not significantly aligned with the photospheric network—they are generally situated above the dark internetwork photosphere. They form compact points or corridors, often without an obvious signature in the underlying photosphere. We argue that these sink points can either be concentrations of closed field footpoints associated with minor magnetic elements in the internetwork or concentrations of an upward-aligned open field. The link between the coronal velocity and magnetic fields is strengthened by comparison with a magnetic extrapolation, which shows several general and specific similarities, thus the velocity maps offer a valuable additional constraint on models.

Unified Astronomy Thesaurus concepts: Quiet solar corona (1992); Quiet solar chromosphere (1986); Solar magnetic fields (1503); Solar atmospheric motions (1478)

Supporting material: animation

1. Introduction

Due to observational limitations, there are large uncertainties of the coronal magnetic field topology above the quiet Sun. Reliable estimates of the magnetic field strength from spectropolarimetric observations currently depend on exceptional observations of high signal (Kuridze et al. 2019) and are particularly challenging for the quiet corona (e.g., Khomenko et al. 2003). Within active regions (AR), systems of large and bright loops can be observed in the extreme ultraviolet (EUV) or X-ray, providing a comparison with magnetic models, including quantitative constraints in some cases (Aschwanden 2013). Above the quiet Sun, the structure of the low coronas as observed in EUV is bereft of distinct and bright coronal loops, leading to uncertainty.

Insight into the quiet Sun coronal topology and connection to the lower atmospheric layers is dependent largely on model extrapolation, constrained by observations of the photospheric and chromospheric magnetic fields and their time evolution (Bellot Rubio & Orozco Suárez 2019). Convective flows of photospheric granules are observed to form coherent supergranular cells of motion with typical diameters of 32 Mm (45") (e.g., Tian et al. 2010; Noori et al. 2019). A comprehensive review is given by Rincon & Rieutord (2018). Their boundaries are regions of convective downdraft that form lanes of magnetic concentrations that coincide with the bright chromospheric network observed in the UV continuum. Schrijver & Title (2003) showed, using arguments based on a potential field magnetic model, that around half of the field may be rooted in the darker internetwork regions, with the other half arising from the network and closing into the internetwork. Wiegelmann et al. (2010) found that most quiet Sun magnetic loops that reach midchromospheric heights or higher have one footpoint in the strong magnetic fields of the network, with the other footpoint in the weaker internetwork regions. A schematic that helps visualize these connections is Figure 16 of Wedemeyer-Böhm et al. (2009), which also gives a comprehensive overview of the field. We also refer the reader to the detailed review of Wiegelmann et al. (2014) and Section 5 in particular.

This work uses the motion of faint propagating disturbances (PDs) in time series of EUV images to gain observational insight into the distribution of the quiet Sun coronal magnetic field. The Time Normalized Optical Flow (TNOF) method to enhance and characterize the PD motions was first described by Morgan & Hutton (2018), with a more simple and efficient approach described by Morgan & Korsos (2022). The amplitudes of the PD are very faint—at most ≈4 DN s⁻¹, or less than 2% of the background signal. They are ubiquitous and continuous, appearing quasi-periodically and showing a preferential direction of motion over local regions of the corona. Past studies of PDs showing similar characteristics include Stenborg et al. (2011), who state that the disturbances are a coronal phenomenon that exists permanently everywhere, and Wang et al. (2009), who found PDs in a fan-like loop structure. The propagation velocities are on the order of tens of km s⁻¹ and have quasi-periodicities, or repetition times, of a few minutes. The PDs are usually interpreted as slow magnetoacoustic waves, with some studies emphasizing...
propagation along an open magnetic field (Stenborg et al. 2011). The events presented by Morgan & Hutton (2018) were generally fainter compared to these other studies, and PDs were found in closed field structures in an active region and quiet Sun. Sheeley et al. (2014) used running difference images and time–distance maps to show “flows” in active regions and within cellular plumes. They describe the global character of these apparent flows, particularly within the context of widespread cellular plumes. We note that the propagating disturbances that they describe included events considerably brighter than those revealed by the TNOF method, and some of the examples had considerably higher speeds (≈90 km s$^{-1}$, compared to below 50 km s$^{-1}$ for TNOF).

2. Coronal Velocity Field

The TNOF method ingests a time series of solar atmospheric images and produces velocity vector maps (Morgan & Hutton 2018; Morgan & Korsós 2022). The method is applied here to the 304 and 193 Å EUV channels of the Atmospheric Imaging Assembly (AIA; Lemen et al. 2011) on board the Solar Dynamics Observatory (SDO; Pesnell et al. 2012). The signature of faint PDs is enhanced relative to the background through the use of a time-normalizing process applied to the calibrated time-series signal. A Lucas–Kanade algorithm is utilized as an optical flow method to trace the motion of the PDs. In this work, the period of study is between 2018 October 27 12:00 UT and 14:00 UT. There are no substantial eruptions or flares during this period. The choice of a 2 hr period is a compromise between gaining the statistics necessary to cleanly characterize the velocity field and minimizing the effects of large-scale motions such as differential rotation, or other changes as described by Morgan & Korsós (2022). The region of study is within $\pm 250''$ from the disk center (relative to Earth) in both $x$ and $y$, shown as the boxed red regions in Figures 1(a) and (b) for 304 and 193 Å, respectively, with more detail shown in Figures 1(c) and (d). The region is mostly quiet Sun, with a small, decaying, equatorial coronal hole in the southwest, which appears dark in the 193 Å image. This dark region was a clear equatorial coronal hole in previous rotations, but by 2018 October 27 has shrunk in width.

The movie accompanying Figure 1 shows the time series of 304 and 193 Å time-normalized and noise-reduced images. The movie shows complex patterns, which are difficult to decipher, although they give a clear sense of consistent and repetitive motion. The Lucas–Kanade algorithm, applied to find the best least-squares fit to the $x$ and $y$ velocity components at each pixel over the 600 time steps, reveals a coherent structure that must underlie these complex patterns. These velocities are interpreted as the dominant direction and magnitude of the motions over the 2 hr of observation. The magnitude of the velocities ranges from 0 to 25 km s$^{-1}$ for 304 Å with a most probable speed of 5 km s$^{-1}$. For the 193 Å channel, the speeds range from 0 to 70 km s$^{-1}$, with a most probable speed of 15 km s$^{-1}$.

Figures 2(a) and (b) show the velocity vectors for the 304 and 193 Å channels respectively, superimposed on the background intensity images. In the 304 Å velocity field, there is a general pattern of flow lines starting (red) and ending (blue) from points, or narrow corridors, of high field-line density. The flow lines between these sources and sinks form cells, or sectors, of coherent flows of approximate diameters 50”. Flow lines do not necessarily form and end at the same region—flow lines from a single source can lead to two or more different sink regions. The 193 Å channel velocity field shown in Figure 2(b) has a similar structure of coherent cells, but they are generally larger, meaning coherent flows over larger areas. Some of the 193 Å flow systems are considerably larger than 100”. For example, the dark coronal hole is a source of flows that reach the neighboring quiet Sun.

The panels of Figure 2(c) show greater detail of four selected regions of the 304 Å velocity field, each of size 70” × 70”. The first example (top left) shows a clearly formed cell with a dense sink region in the center. The flow lines converge from all directions into this central sink. Some originate from a point-source region in the lower left of the area, others arise from a dense corridor aligned north–south toward the left of the area. The top-right panel shows a similar cell structure, which has a central sink region, and also a neighboring point-source region in the top left. The bottom-left panel of Figure 2(c) shows an example of an extended, narrow sink corridor that meanders from the bottom-left to the top-right corner. The bottom-right panel shows a central sink region where the incoming flow lines have a consistent pattern of rotation around the central sink. In this case, the field lines describe one complete rotation from their source to their center destination. There are many examples of such rotations in the main velocity field of Figure 2(a) and can be compared to the large distinct vortex described in Section 7 and Figure 20 of Morgan & Hutton (2018). A more detailed study may show that these rotational structures are linked to certain features on the photosphere, for example, persistent rotational regions associated with supergranular vertices (Requerey et al. 2018).

The four panels of Figure 2(d) show details of four selected regions from the 193 Å velocity field. The two top panels show two typical cell regions. The first, on the left, is a clear cell structure that has an extended sink corridor in the center, with inwardly converging flow lines. The flow lines emerge from two narrow source corridors that form the left and bottom boundary of the cell. The top-right panel shows another cell example, which has a point-like sink region in the center, with three neighboring source regions that are more localized than the extended corridors in the first example. The bottom-left panel is an example of an extended corridor of convergence, and the bottom-right panel is an example of a rotated source region. These rotated structures are rare in the 193 Å channel compared to the 304 Å. We speculate that this is due to the corona being less closely connected to the photosphere compared to the cooler layers observed by the 304 Å channel, thus the smaller cell structures in the 304 Å channel may be closely associated with a rotating region in the photosphere, causing a degree of rotation at that height. The larger cellular structures in the 193 Å channel may bridge above the smaller cells of the 304 Å channel and be less prone to the rotation of the photosphere at smaller spatial scales.

In both channels, the flow lines that feed into or out of dense corridors of divergence/convergence tend to approach the corridors at a similar angle. That is, on the approach to the corridor, a flow line tends to join the corridor at an acute angle that is similar to other flow lines at that side of the corridor. Flow lines that approach from the other side of the corridor follow the same pattern, with the angle of approach reflecting the opposite side—giving a pattern akin to a fern leaf. This suggests that the flow tends in one direction along the corridor.
The bottom- and top-left panels of Figure 2(d) show examples of fern-leaf-shaped divergence corridors for the 193 Å channel. In the 193 Å channel, the flow lines within the coronal hole area (the 193 Å dark region in the southeast) link to neighboring brighter regions, and in the 304 Å channel, there is no general difference in the pattern of flow lines within this region compared to the quiet Sun. We would expect the center of the equatorial coronal holes to be dominated by an open magnetic field and a different flow pattern from that in quiet Sun regions, but the results seen here may relate to the fact that the coronal hole has decayed. The coronal hole is discussed further in Section 5.

The top row of Figure 3 shows a simplified representation of the complicated flow fields. The blue and red lines represent certain regions where the direction of the flow field changes direction abruptly. The direction of the flow field at each pixel is given by the angle $\Omega = \arctan(v_y/v_x)$. The Sobel edge enhancement operator is applied to this angular image to give a value at each pixel: Very high values are found at regions where the angle in velocity direction changes abruptly—both the red and blue lines in the bottom row of Figure 2 correspond to high values. The red (blue) colors denote where these regions of abrupt angular change have positive (negative) divergence. For convenience, we denote the regions of angular discontinuities and positive or negative divergence $S^+$ and $S^-$, respectively. The blue lines overlie the points and narrow corridors where flows converge from surrounding areas (sinks), while the red lines overlie the points and corridors where flows diverge to surrounding areas (sources).

Figure 3(c) shows the $S^+$ distribution (flow sources) for the 304 Å (red) and 193 Å (green) velocity fields. There is a correlation between the two distributions across most of the region, with a spatial alignment significance (see Appendix) of $2.7\sigma$ and a percentage significance of 100% (i.e., the alignment score is higher than all random cases). The 193 Å $S^+$ forms longer, more coherent, lines than the 304 Å, thus showing the
larger-scale coherence of the 193 Å flow fields, and the general trend for smaller-scale structure in the cooler channel, as can be seen visually in Figures 2(a) and (b). In Figure 3(b), which shows the \(S^+\) distribution (flow sinks) for the 304 Å (blue) and 193 Å (green) velocity fields, the fields are in broad agreement in some regions, but the spatial match is overall weaker with a spatial alignment significance of 1.7\(\sigma\) and percentage of 95\%. Thus, the cooler 304 Å channel and hotter 193 Å channels are more likely to share common source regions with their PDs but less likely to share alignment between sink regions (or where the PD flow lines end).

Figures 3(e) and (f) show greater details of the velocity vector fields for 304 and 193 Å, respectively, in a small region near the disk center. These figures emphasize the fact that both channels can share the same source and sink regions, but that the cooler 304 Å channel tends to have more source and sink regions and has shorter flow paths with a higher curvature between these regions. For example, both channels share a dominant source near the region center. They also have a sink point to the top right \((x, y = 45\arcsec, 5\arcsec)\). This sink point shows rotation only in the 304 Å channel.

3. Comparison with Photospheric Observations

Figure 4(a) shows an observation of the region of interest by the AIA 1700 Å channel, where the ultraviolet continuum is
Figure 3. Top row: velocity vector maps shown without color or background image for the (a) 304 and (b) 193 Å channels. The red and blue lines show where there is a large change in direction of the local velocity vector, with red corresponding to positive divergence ($S^+$, or source of flows) and blue corresponding to negative divergence ($S^-$, or where flows converge). Middle row: (c) $S^+$ regions for the 304 Å (red) and 193 Å (green) velocity fields. These are regions of large angular change and positive divergence in the velocity vector fields, so trace out the center of flow source regions. (d) $S^-$ regions for the 304 Å (blue) and 193 Å (green) velocity fields. These trace regions of large angular change and negative divergence, or the corridors and points where flows converge. Bottom row: further detail of the velocity vector field for the (e) 304 and (f) 193 Å channels, for the small region near the disk center boxed in panels (c) and (d).
dominated by the temperature minimum/photospheric intensity. These data show the patchwork of dark internetwork regions bounded by the bright network. Analysis of a time series of such images taken between 2018 October 27 12:00 to 14:00 UT show changes only to small-scale features, while the brightest large-scale network patterns remain fairly stable. The negative of the same data (black = bright) is shown as the background image of Figure 4(b), with the detected brightest network patterns highlighted in green. Figure 4(c) compares the bright photospheric network (green) with the AIA 304 Å velocity field characterization of $S^+$ (red, positive divergence or sources) and $S^-$ (blue, negative divergence or sinks). Figure 4(d) shows the same comparison for the AIA 193 Å velocity field.

Figure 4. (a) Observation of 2018 October 27 13:00 UT of the region of study by the AIA 1700 Å channel, showing the photospheric UV continuum. (b) The negative of the AIA 1700 Å channel intensity (white = low intensity), with the brightest network features highlighted in green. (c) Comparing the UV network (green) with the AIA 304 Å velocity field characterization of $S^+$ (red, positive divergence or sources) and $S^-$ (blue, negative divergence or sinks). (d) As panel (c), but for the AIA 193 Å velocity field.
mostly negative, field in the HMI data. The 193 Å sink features are generally not closely aligned with photospheric enhancements but can sometimes coincide. For this same region in the 304 Å channel, shown in panel (c), there is less obvious correlation, although source features appear more likely to coincide with enhanced photospheric field compared to sinks. Figure 5(e) shows a close alignment between a loop-shaped 304 Å source feature and the photosphere. Most of the sink features are not aligned with the enhanced field, and indeed, one prominent sink feature sits within the looped source feature. A larger loop of sink points surrounds the inner source loop. The same region in 193 Å, shown in Figure 5(f), also shows a close alignment between some source features and the photosphere, but the pattern is not as clear as the 304 Å case.

Figure 5. A comparison of photospheric magnetograms calculated from HMI observations of 2018 October 27 13:00 UT with the 304 (left column) and 193 Å (right column) velocity fields. The top row shows the velocity fields superimposed on the HMI magnetogram for the whole region of study. The middle row shows the source (red) and sink (blue) features of the velocity fields superimposed on the magnetogram for a small region near the disk center. The bottom row shows another small region to the south of the disk center.
near the disk center. The extrapolated Figure 6. The Astrophysical Journal Letters, 933:L27 (13pp), 2022 July 10

maximum extrapolated height of 0.2 extrapolation, based on the HMI magnetogram. Our code for the photosphere. In this subsection, we extend this the coronal velocity data, it is obvious that there is a link between the distribution of the photospheric potential, including two potential regions shown in the middle row of Figure 5. For efficiency, we resize the magnetogram to a quarter of the number of pixels, so that each new pixel is the local average of four pixels of the original. To avoid edge effects, the extrapolation area extends by 10″ beyond the displayed area at all margins, and the photospheric input to the extrapolation extends well beyond this. The extrapolation volume extends to 0.2R⊙ above the photosphere. We use all of the magnetogram pixels to calculate the potential field, not just enhanced sources, and we do not fit the photospheric field to a smooth function. Thus, the potential at a given coronal point in the extrapolation volume is calculated from all photospheric points within the visible horizon.

Figure 6(b) shows the result of the PFSS extrapolation. The field lines are traced in the 3D volume, and their coordinates are transformed into the observer’s field of view. There are many similarities between the PFSS and velocity fields, as well as some major differences. On a general level, the PFSS field is cellular, with dense concentrations of footpoints aligned with stronger photospheric magnetic elements. The field lines at greater heights (colored green/yellow/red) can bridge over closed underlying systems at low heights (colored black). Furthermore, while many field lines have one footpoint in a dense source and the other in a low-density internetwork region, lines can also join in dense, narrow corridors, similar to the fern-leaf patterns seen in the velocity fields. We can thus find most of the general features of the velocity fields in the PFSS extrapolations.

Beyond these general similarities, there are also specific features that are shared between the PFSS and the 304 Å velocity field, including

1. A very similar distribution of field lines within, and surrounding, the central prominent feature at x, y = [−10, −20]°. This is also similar to the 193 Å velocity field.
2. The cell systems centered at [−35, 0]°, and [−55, −15]°, and their connection to the central prominent feature and each other.
3. A cross-shaped meeting of field lines at the boundary of distinct cell systems at [−10, −55]°. Two other similar systems are seen at [0, 45]° and [35, 25]°. The corresponding features in the PFSS extrapolation are at slightly different locations.

We note that the 304 Å velocity field contains several rotating features: Two of them are seen here centered at [−50, −60]° and [45, 5]°. There is no corresponding spiral pattern in the PFSS extrapolation. That there is no spiral structure in the magnetic field of the PFSS model is expected because the model has no time dependence and is force free.

5. The Coronal Hole

This section makes a more detailed analysis of the narrow coronal hole seen in the southeast of the region of study. In particular, we expect coronal holes to be dominated by an open field and further expect that field to be expanding superradially from the central regions of the coronal hole, which seems to be in contradiction to the velocity field patterns seen in Figures 2(a) and (b) and shown in greater detail in Figure 7(d) for the 193 Å channel.

We first define a boundary to the coronal hole using a differential emission measure (DEM) analysis. The method we use is the Solar Iterative Temperature Emission Solver (SITES, Morgan & Pickering 2019; Pickering & Morgan 2019), and the input data are AIA/SDO data from the seven EUV channels. The resulting DEM, at a cool temperature of 0.6 MK, is shown in Figure 7(a). Figure 7(b) shows the fractional emission measure (FEM), which is the emission at that temperature
divided by the total emission summed over all temperatures. The map shows a clear region of enhanced FEM within, and surrounding, the coronal hole. The hole boundary, shown as the red contour, is defined by any regions that have an FEM over 3.5% and with the number of connected pixels larger than a few hundred. Figure 7(c) plots the coronal hole boundary over the HMI magnetogram. Visually, there is no discernible difference between the photosphere within the hole and outside in the surrounding coronal hole. Figure 8(a) shows that the histograms of the photospheric magnetic field inside and outside the coronal hole are very similar—indeed, their mean and standard deviations are close to identical. It is only when one histogram is subtracted from the other that we see a small bias toward negative polarities within the coronal hole, as shown in Figure 8(b).

We extract the photospheric field values for a line cutting east–west across the coronal hole, shown as the horizontal blue line in Figures 7(c) and (d). This field is shown in the lower
only the projected (or plane-of-sky) velocities. Nevertheless, the flow lines give a unique proxy of the quiet Sun coronal magnetic field structure based directly on EUV coronal observations—information that is currently impossible to gain without magnetic modeling. The pattern seen in the quiet Sun region of Figure 2, of cells, or sectors, of flow line systems arising from and ending in points and narrow corridors, leads to the hypothesis that the magnetic field topology has a similar sectorial structure.

In the lower atmosphere, corresponding to the 304 Å channel, we expect the closed magnetic structures that form the quiet Sun corona to have generally smaller structural scales than the overlying coronal field traced by the 193 Å channel, and this is what is seen in the PD velocity fields. In the cooler 304 Å channel, the cell diameters are typically \( \approx 50'' \), while the hotter 193 Å channel tends to have larger cell sizes, with some larger cells of diameter 80'' to larger than 100''. The coronal field traced by the 193 Å channel can share common sources and sinks with the 304 Å channel but can often bridge over one or more cells in the cooler 304 Å channel.

The cells tend to have central point-like, or corridor-like, source regions, with neighboring systems of sink points or corridors forming their boundaries. Some cells show a clear rotational motion. These are common in the 304 Å channel and rare in the 193 Å channel. The apparent rotational flows suggests that the magnetic field may be twisted due to the coherent large-scale rotation of areas of the underlying photosphere. The projected fern-leaf shape of the narrow sink/source corridors suggests that there is a dominant direction of flow along the narrow corridors and a dominant orientation of the magnetic field along the narrow corridors.

The comparison with the underlying photospheric UV intensity, and with photospheric magnetograms, shows that the sources of the field lines tend to overlie the bright network, while their sinks tend to lie in the darker internetwork regions. This result is important. It reinforces the hypothesis that the velocity fields are a tracer of magnetic fields and is consistent with the accepted model of the bulk of the quiet Sun magnetic field concentrated in network regions. Furthermore, if the PDs are slow magnetoacoustic waves, then these brighter UV network regions, and enhanced magnetic elements, are conducive to the production of waves. If the internetwork regions were equally productive, then we would not see a clear preferential direction of the PD flows from the network and toward internetwork regions. Certainly there is much further work that can be done to investigate this relationship, including a more detailed comparison with the photospheric and lower-chromospheric magnetic field distribution, and a comparison with the results of motion tracking in the photosphere (e.g., Chian et al. 2019).

The most surprising result is the distribution of the flow sinks (convergence regions). That the flow sources tend to emerge from dense, narrow points or corridors, and that these tend to align with bright network regions, is consistent with general models of the quiet Sun magnetic field. The source field arising from the network boundaries is expected to expand with altitude, filling the transition region and low corona, with the field forming the basic building blocks of the quiet Sun corona. However, our results show that the opposite footpoints (or sink footpoints) of these closed loop systems are also distributed in dense narrow points or corridors, similar to their source footpoints. That is, the field arising from the network...
In the case of a zero two strong positive elements in the right column of Figure 10. The experiment is repeated with a random source, the large sources. Despite the weakness of this photospheric intensity or in photospheric magnetograms—they are situated within the weak field of the dark internetwork regions.

Support for the presence of concentrated sink points/corridors in the quiet Sun internetwork regions can be given by simple experiments with a two-dimensional PFSS model. In an otherwise zero field, the footpoints diverge from, and converge to, distinct, small areas forming points or corridors. In contrast to the source regions, the sink regions are not aligned with the photospheric network boundaries, and there is not always a distinct signature of the sink regions in the UV photospheric map of standard deviation 1% of the large sources. Despite the weakness of this photospheric random source, the field at low heights is perturbed, as shown in Figure 10(b). We now add a weak negative element of amplitude 6% of the strong elements, equidistant between them. The field is now quite strongly perturbed at low to medium heights, and several field lines link the strong positive element to the weak negative element, as shown in Figure 10(c)—leading to a concentration of field lines at the position of the small negative enhancement. The experiment is repeated with two strong positive elements in the right column of Figure 10. In the case of a zero field, or weak random field, outside of the strong elements (Figures 10(d) and (e)), the coronal field has a concentration of upwardly pointing open field at the center of the system. When a weak negative element is placed in the center (Figure 10(f)), we have a strong concentration of both a downwardly pointing closed field as well as the open field. We argue that such configurations may be common in the quiet Sun and can explain the dense sink regions for our velocity fields. In the case of Figure 10(d), the central region between the two strong positive sources has a dense concentration of upwardly aligned open fields, and this would appear as a dense sink region in a coronal PD velocity field. Relatively weak enhancements in the internetwork region can also lead to concentrations of closed field lines in the internetwork, which would also appear as sink regions in the velocity fields (Figures 10(c) and (f)).

We note that a recent detailed observational study of the magnetic configuration of a supergranule by Robustini et al. (2019) suggested that the chromospheric field lines tended to point inward from the supergranule boundary and may form a canopy above the unipolar interior region. Furthermore, they found a persistent internetwork small brightening coinciding with a distinct blueshifted (downflow) feature in the line-of-sight velocity of the Ca II K line. Chian et al. (2019) showed repelling Lagrangian coherent structures concentrated at the center of a supergranule. Thus, central regions in the internetwork are special—they are central source regions of local supergranular-scale motions, and their properties may lead to a higher concentration of overlying atmospheric magnetic field lines.

Our next efforts are aimed to better understand the connection between the velocity fields and the atmospheric magnetic field. We will combine our PD tracking method with spectroscopic observations of EUV lines and will focus on whether the source and sink regions coincide with regions of Doppler shifts or other distinguishing properties. We plan to create disk-center velocity fields for AIA/SDO during periods when other spacecraft hosting EUV imagers (e.g., Solar Orbiter) are 90° to Earth, enabling a
comparison of the equatorial off-limb structure in EUV with the velocity field distributions from the SDO viewpoint. We are also interested in comparing our coronal flow fields with photospheric and chromospheric flow fields. In the longer term, an exciting possibility is to use our results as a proxy for the projected plane-of-sky distribution of coronal magnetic fields and use this as an empirical constraint on magnetic extrapolation models. This can be particularly useful for the quiet Sun and coronal holes, where the EUV emission does not trace systems of clear loops as is seen in active regions.

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Appendix
Quantifying the Agreement between Two Binary Spatial Distributions

Two-dimensional masks $M_0$ and $M_1$, both with $n$ pixels and the same shape, contain values of only zeros and ones, with the ones (zeros) corresponding to some definition of true (false).

For example, the blue and green regions of Figure 3(a) correspond to true values for $M_0$ and $M_1$, respectively. $M_0$ is convolved with a narrow two-dimensional Gaussian kernel $k$ giving a smoothed mask $S_0$:

$$S_0 = M_0 \otimes k,$$

and the same for $S_1$. The purpose of the convolution is to spread narrow structures in the mask, enabling some overlap between closely aligned structures that may not exactly overlap in both masks. In this work, we use a sigma width of 1 pixel for $k$. $P_{01}$ is the product of $S_0$ and $S_1$: $P_{01} = S_0 S_1$, and a mask $N_{01}$ is defined as $N_{01} = P_{01} \geq t$, where $t$ is a small threshold. In this work, $t = 0.05$. Finally, a score $c_{01}$ for the agreement between the two masks $M_0$ and $M_1$ is given by

$$c_{01} = \frac{2n \sum N_{01}}{\sum N_{00} + \sum N_{11}},$$

where the summation is over all pixels. The denominator is a normalizing factor, where $N_{00} = P_{00} \geq t$ and $P_{00} = S_0 S_0$ (and similar for $N_{11}$). The denominator ensures that $c_{01} = 1$ for the case of $M_0 = M_1$ and $0 \leq c < 1$ for the general case.

A random test is used to quantify the significance of the score $c_{01}$. $M_0$ is segmented into a set of coherent regions

Figure 10. Experiments with a simple two-dimensional potential magnetic field. The left column shows cases with two strong magnetic sources, one positive on the left, and one negative on the right. The right column shows cases with two strong positive sources. In each panel, the green line shows the photosphere. Below this green line, the red line shows the strength of the source (photospheric) field, with the location of the two strong sources shown by vertical blue lines. The range of the source field is limited to small values around zero in order to show small variations so that the left and right source peaks are heavily curtailed. The top row shows the case where there are two strong sources and zero field elsewhere. The middle row adds small random photospheric variations, with standard deviation amplitudes of 1% of the amplitude of the two strong sources. The bottom row has the two strong sources, random variations, and a small central negative source with amplitude 6% of the two strong sources. The position of this small negative source is indicated by the vertical blue line, equally spaced between the two strong sources.
(groups of connected pixels). Each group’s centroid is translated to a random location, with the connected pixels rotated by a random angle around this new centroid. If coordinates of the translated/rotated region lie outside of the bounds of $M_0$, those coordinates are wrapped to the opposite boundary. Thus, a new random mask is created, which has similar characteristics to the unmodified mask, composed of the moved and rotated connected regions of $M_0$. A score $c$ is calculated between this random mask and $M_1$. This process is repeated many times (1000 for this work), with the score $c$ recorded for each case. The resulting normal distribution of $c$ allows a test of the significance of $c_{01}$ by evaluating the mean $m$ and standard deviation $\sigma$ of $c$ and calculating $c_{01}$’s distance from $m$ in units of $\sigma$. More simply, we can assign a percentage significance by counting the number of cases of the random distribution with a lower score than the actual distribution. For example, if 900 of the 1000 random cases have a lower score than the actual, then the spatial agreement percentage is 90%.

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