Modeling of Refractive Index Sensing Using Au Aperture Arrays on a Bragg Fiber Facet

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Abstract: A finite-difference-time-domain (FDTD) approach is undertaken to investigate the extraordinary optical transmission (EOT) phenomenon of Au circular aperture arrays deposited on a Bragg fiber facet for refractive index (RI) sensing. Investigation shows that the choice of effective indices and modal loss of the Bragg fiber core modes will affect the sensitivity enhancement by using a mode analysis approach. The critical parameters of Bragg fiber including the middle dielectric RI, as well as its gap between dielectric layers, which affect the EOT and RI sensitivity for the sensor, are discussed and optimized. It is demonstrated that a better sensitivity of 156 ± 5 nm per refractive index unit (RIU) and an averaged figure of merit exceeding 3.5 RIU−1 are achieved when RI is 1.5 and gap is 0.02 μm in this structure.

Keywords: Optical fiber sensors; surface plasmon resonance; periodic array; refractive index sensing; finite-difference time-domain

1. Introduction

Surface plasmon resonance (SPR) is the resonant oscillation of free electrons excited by light at the metal/dielectric interfaces [1]. Due to the interfacial nature of SPR, refractive index (RI) sensing for quantitative analysis of chemical reactions and biological interactions has become one of the most promising applications of nanoplasmonics. Thus, SPR is adopted in many optical tools for measuring light-matter interactions onto the surface. In the first place, SPR on metamaterial absorbers as sensing has been focused on optimizing the metallic nanoparticle geometries to improve the sensor performance [2–5]. Afterwards, SPR on periodic metallic structures has attracted increasing interest since the observation of extraordinary optical transmission (EOT) phenomenon being first demonstrated by Ebbesen in 1998 [6]. A new generation of the optical sensor based on EOT has been regarded as a promising solution for RI sensing purposes. Like that, exploring the SPR electromagnetic field localization properties for sensing has been proposed to overcome the limitations in operation and beat performances of other optical detection approaches [7]. In contrast to prism-based SPR sensors with Kretschmann configuration [8], the combination of SPR and optical fiber would have the possibility for far extending the scope of SPR utilization in biological...
and chemical communities. Over the past few years, many fiber-based SPR sensors have been reported, including SPR sensor configurations with multimode, single mode, and D-shaped fibers coated with a thin metallic layer [9–11]. These kinds of sensors require a complex manufacturing process, and their sensing performances are not good. Owing to the impressive progress in the nanofabrication technology, many researchers have pursued this idea in a quest to create sensitive RI sensors by fabricating an apertures array integrated on optical fiber facet. More recently, there have been many successful attempts to realize SPR based EOT sensors in optical fibers facet [12–16]. However, these early proposals offer preliminary designs with little theoretical or experimental evidence to show that the sensing performance of optical fiber sensors would be enhanced by a metallic nanostructure. We would like to develop some new types of nanostructures that can improve the analytical figures of merit (FOM), such as detection limits and sensitivity, relative to the commercial systems.

In this paper, we report a novel device, which is composed of Au aperture arrays directly fabricated on the core-cladding Bragg (C-C Bragg) fiber facet and it is applied as an optical sensor based on EOT. We begin with the comparative analysis of effective indices ($\varepsilon_{\text{eff}}$) and loss of the core modes for C-C Bragg fiber and C-C fiber by using the mode analysis approach. Here, the effect of crucial parameters of C-C Bragg fiber including the middle dielectric RI ($n_{\text{M}}$), as well as its gap ($t_g$) between dielectric layers on the EOT, is analyzed and optimized numerically using the finite-difference-time-domain (FDTD) method. Moreover, by tuning the above two parameters, we can obtain the best EOT property and increase its sensitivity. We hope our findings provide guidance to fundamental research of a high-sensitivity integrated optical fiber sensor based on EOT.

### 2. Device structure and the analysis method

The schematic diagram of the proposed optical sensor with Au circular aperture arrays on a C-C Bragg fiber facet (RI of core is denoted by $n_1$; RI of cladding is denoted by $n_2$) is shown in Fig. 1(a). Au aperture arrays are placed onto the fiber facet, where the pitch of the square lattice is denoted by $A$, $A=0.4 \mu m$ and the diameter of air aperture is denoted by $d_a$, $d_a=0.2 \mu m$. The Bragg fiber, where the high index central region (acts as the core) is surrounded by concentric layers of alternate low refractive index materials, is shown in the top view structure of Fig. 1(b). Figure 1(b) shows the refractive index variation with respect to the radial distance for the rectangular solid core Bragg fiber, in which $d_c$ is the diameter of the solid core region, and $n_{\text{M}}$ and $t_g$ are the RI of two different consecutive cladding and its gap, respectively.

Afterwards, we use the commercial full-wave electromagnetic field simulation software package, FDTD Solutions and MODE Solutions (Lumerical Solutions Inc., Canada) [17] to investigate the modal profiles, EOT, and sensing performances of the proposed sensor, which uses finite difference approximation in both time and space domains to calculate the Maxwell’s curl equations step by step. Initially, Au aperture arrays are filled with air, $n_{\text{M}}=1.0$. RIs of the C-C fiber are taken as $n_1=2$ and $n_2=1.5$, respectively. The dielectric constant of Au in the visible and near-IR region is defined by the Drude model described as [18]

$$
\varepsilon_{\text{Au}}(\omega) = \varepsilon_{\infty} - \frac{\omega_p^2}{\omega^2 + i \gamma \omega}
$$

where $\varepsilon_{\infty} = 9.75$ is the dielectric constant of Au at high frequency, $\omega_p = 1.36 \times 10^{16}$ is the plasma frequency of Au, $\omega_s = 1.45 \times 10^{13}$ is the scattering frequency of electron, and the data were given by Johnson and Christy [19]. In our calculation, we use mesh sizes ranging from 1 nm to 4 nm. For the calculation of the transmittance, the structures are excited by a mode sources packet composed of normally incident single fundamental mode waves (with the electric field pointing along one of the axes of the square array) and all frequencies of interest in a small solid angle centered around the normal.
direction along the $z$-direction. Infinite periodic aperture arrays are simulated by applying Bloch conditions at the boundaries of the unit cell and imposing “uniaxial perfectly matched layer (PML)” at surfaces parallel to the Au film. The calculated zero-order transmission spectra around the circular apertures are shown in Figs. 3(a), 3(b), Figs. 4(a), 4(c), and Fig. 5(a).

Fig. 1 Schematic diagram of the optical sensor with Au circular aperture arrays on a C-C Bragg fiber facet: (a) 3D view of the structure and (b) top view of the structure and RI variation with radial distance of rectangular solid core Bragg fiber.

3. Results and discussion

In order to gain a deeper understanding, we analyze the dependence of the optical sensor mode’s $n_{\text{eff}}$ for C-C Bragg fiber and C-C fiber using a finite-difference eigenmode (FDE) solver of MODE Solutions. Figure 2(a) depicts the variation tendency of their real parts of $n_{\text{eff}}$ as a function of the wavelength. The real part of $n_{\text{eff}}$ decreases with increasing wavelength corresponding to C-C Bragg fiber and C-C fiber. And it is found that the latter decays faster. The illustration shows their corresponding index profile in $x$-$y$ plane. By studying comparatively, we suggest that C-C Bragg fiber is the optimal structure. To test the idea, we also analyze the dependence of the optical sensor mode’s modal loss for C-C Bragg fiber and C-C fiber. The fundamental mode is analyzed to investigate the propagation loss. By using the imaginary part of effective index $\text{Im}(n_{\text{eff}})$, the propagation loss is defined as [20]

$$\alpha = 40\pi \text{Im}(n_{\text{eff}})/[\text{ln}(10)\lambda]$$

$$\approx 8.686k_0 \text{Im}(n_{\text{eff}})10^4 \text{ dB/cm}$$

(2)

where $k_0 = 2\pi/\lambda$ is the wave number in the free space, and the wavelength and $\lambda$ is in micron.

Figure 2(b) shows the dependence of the modal loss spectra of the fundamental mode for C-C Bragg fiber and C-C fiber. It is found that the leaky energy loss exhibits an upward positive enhancement trend for C-C Bragg fiber and a downward negative enhancement trend for C-C fiber, which indicates the effective occurrence of SPR in C-C Bragg fiber.

To investigate the RI sensing property of the proposed sensor, we firstly use an FDTD numerical simulation to model the EOT spectra of Au aperture arrays on C-C Bragg fiber and C-C fiber two facets. Structure parameters include $n_1=2$, $n_2=1.5$, $n_{\text{air}}=1.8$, and $t_g=0.03\mu$m. Then, their RI sensing properties are analyzed. The simulated results are presented in Fig. 3. Figure 3(a) clearly shows the obvious difference of zero-order transmittance spectra in the wavelength range of 0.4 $\mu$m and 0.65 $\mu$m with two different structures. In the first place, it is found that their peak intensity ($T_{\text{peak}}$) and full-width-at-half-maximum (FWHM) values are different. Comparing two different $\lambda_{\text{peak}}$, 551 nm and 560 nm, it is found that a higher and narrower solid-line peak is obtained with C-C Bragg fiber. It shows that the solid-line $T_{\text{peak}}$ value is up to 5 arbitrary units (≈40%) more than that of dashed-line. The solid-line FWHM value is 31 nm,
less than 47 nm of dashed-line FWHM value. Meanwhile, it can be found that for $\lambda_{peak}$ of 551 nm, the $|E|$ distributions in x-y plane are much stronger than that at the $\lambda_{peak}$ of 560 nm, with a balanced view, C-C Bragg fiber structure shows a better EOT performance. Then, we perform an RI sensing analysis of the optical sensor with C-C Bragg fiber and C-C fiber by calculating their zero-order transmission spectra in $n_1=1.30$ and $n_1=1.38$, as shown in Fig. 3(b). The inset of Fig. 3(b) shows the $|E|$ distributions of fundamental core mode and SPP mode in x-z plane at their corresponding $\lambda_{peak}$. With a C-C Bragg fiber added, the fundamental core mode and SPP mode strongly couple together, the $T_{peak}$ observably enhances, meanwhile, $\lambda_{peak}$ has a large range redshift ($\Delta=18 \text{ nm} > \Delta=8 \text{ nm}$), which leads to the improved sensitivities in wavelength interrogations. The proposed optical sensor operation is based on the SPR evanescent fields and its interaction with the analytes. In view of the experiment, to determine the sensitivity, gold hole array fiber is equipped with a fluidic channel. The analyte is injected into gold hole array through the flow cell sequentially using a syringe pump. The sensitivity is analyzed by using the $\lambda_{peak}$ interrogation method. The corresponding sensitivities are expressed in [20], which are given in units of nm/RIU

$$S_{(a)} = \frac{\Delta \lambda_{peak}}{\Delta n_i} \text{ (nm/RIU)}$$

where $\Delta \lambda_{peak}$ is the resonance peak shift, and $\Delta n_i$ is the variation of the RI of analyte.
Firstly, $n_{(M)}$ is introduced to optimize the EOT performance. Figure 4(a) plots the calculated zero-order transmission spectra of the sensor with $n_{(M)}$ of 1.5, 1.6, 1.7, 1.8, and 1.9, respectively, when the other parameters remain unchanged. Then, we analyze its sensing performance by calculating the zero-order resonant spectra in a large dynamic range to find the corresponding peak ($\lambda_{\text{peak}}$) (the five-middle peaks connected by a dashed-line). In the following study, we vary $n_{(M)}$ to investigate its influence on $S_{(\lambda)}$, as shown in Fig. 4(b). The maximal value is 87 with $n_{(M)} = 1.5$, as shown in the red-solid-line transmission spectral of Fig. 4(a), where it has a best EOT peak performance. Figure 4(c) plots the calculated zero-order transmission spectra of the sensor with the $t_g$ of 0.01 $\mu$m, 0.015 $\mu$m, 0.02 $\mu$m, 0.025 $\mu$m, and 0.03 $\mu$m, respectively, when the other parameters remain unchanged. Then, we analyze its sensing performance by calculating the zero-order resonant spectra in a large dynamic range to find the corresponding peak ($\lambda_{\text{peak}}$) (the five-middle peaks connected by a dashed-line). In the following study, we vary $t_g$ to investigate its influence on $S_{(\lambda)}$, as shown in Fig. 4(d). The maximal value is 90 with $t_g = 0.02 \mu$m, as shown in
the blue-solid-line transmission spectra of Fig. 4(c), where it has the best EOT peak performance.

![Graph showing transmission spectra](image)

Fig. 5 Sensor performance analysis for (a) calculated zero-order transmission spectral for the sensor in various $n_s$ with $t_{(Au)} = 100\text{nm}$, $n_{(M)} = 1.5$, and $t_g = 0.02\text{µm}$, as a function of the wavelength and (b) dependence of the corresponding $\lambda_{peak}$ on $n_s$, showing the linear fitted result of $\lambda_{peak}$ with different $n_s$.

Above findings advise that through a suitable choice of $n_s$, as shown in the enlarged illustration of Fig. 5(a). Finally, we investigate the RI sensitivity by analyzing the above $\lambda_{peak}$. The corresponding linear fitting lines of $\lambda_{peak}$ with respect to $n_s$ is presented in Fig. 5(b). The regression equations in Fig. 5(b) are as follows:

$$\lambda_{peak} (\text{nm}) = 156n + 365, \quad 1.30 \leq n_s \leq 1.38. \quad (4)$$

The slopes of the equation give an average $S_{(\lambda)}$ of the analytes, i.e., $156 \pm 5 \text{ nm/RIU}$, within the relevant sensing range. The adjusted R-Square values of $\lambda_{peak}$ fitting lines are 0.99375, indicating a high linearity of the optical sensor. For the practical applications, the FOM is another important parameter of the POS to evaluate its sensing performance, which is defined as $\text{FOM} = S_{(\lambda)}/\text{FWHM}$ [21]. In this regard, the averaged FOM values of the POS can reach $3.5 \text{ RIU}^{-1}$.

4. Conclusions

In summary, a study is undertaken to investigate Au aperture arrays deposited on the C-C Bragg fiber facet for RI sensing using the FDTD method. It is demonstrated that the suitable choice of $n_{(M)}$ and modal loss of the core modes for C-C Bragg fiber can increase the sensitivity with mode analysis approach. The effects of $n_{(M)}$ and $t_g$ on EOT phenomenon and $S_{(\lambda)}$ are discussed and optimized, correspondingly. It is found that when $n_{(M)} = 1.5$ and $t_g = 0.02\text{µm}$ in this structure, they yield the best EOT phenomenon, in which $S_{(\lambda)}$ is $156 \pm 5 \text{ nm/RIU}$, and its averaged FOM value is $3.5 \text{ RIU}^{-1}$. This investigation will assist in designing structures that maximize the $S_{(\lambda)}$ of a RI sensing optical device.

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