Causality and the Semantics of Provenance

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Provenance, or information about the sources, derivation, custody or history of data, has been studied recently in a number of contexts, including databases, scientific workflows and the Semantic Web. Many provenance mechanisms have been developed, motivated by informal notions such as influence, dependence, explanation and causality. However, there has been little study of whether these mechanisms formally satisfy appropriate policies or even how to formalize relevant motivating concepts such as causality. We contend that mathematical models of these concepts are needed to justify and compare provenance techniques. In this paper we review a theory of causality based on structural models that has been developed in artificial intelligence, and describe work in progress on a causal semantics for provenance graphs.

1 Introduction

Provenance is a general term referring to the origin, history, chain of custody, derivation or process that yielded an object. In analog settings such as art and archaeology, such information is essential for understanding whether an artifact is authentic, valuable or meaningful. In the digital world, provenance is now recognized as an important problem because it is very easy to silently alter or forge digital information. We already pay a price because of the lack of robust mechanisms for recording and managing provenance: serious economic losses have been incurred due to the lack of provenance on the Web [3], and lack of transparency of scientific processes and results is routinely used to sow confusion and doubt about climate change [25].

Much work on provenance considers the following basic scenario: we have some input data and some complex process that will be run on the input, for example a large program, possibly split into many smaller jobs and executed in parallel or on a distributed system. In this setting, a proposed solution generally records some additional information as the program runs. The additional information is often called provenance and it is supposed to provide an “explanation” showing how the results were obtained.

Of course, this is a loose specification if we do not clarify what we mean by an explanation (apart from whatever provenance information happens to be recorded by the system). There are at least two obvious-seeming choices, neither of which seems satisfactory in practice:

- First, we might record the program that was run along with its input data (and any intermediate inputs such as user or network interactions). This, at least, allows us to rerun the program later and check that we get the same result, and it also allows us to vary the inputs to see how changes affect the output. But this is nearly useless as an explanation, especially for end-users who are not (and should not be expected to be) proficient at debugging black-box systems. Moreover, the inputs and outputs may be huge (for example, gigabytes of climate data), and it may not be possible for users to manually inspect the data. In the longer term, just recording the program is also problematic since the computational environment in which the program runs will change — in some sense, this is also an “input” that we cannot feasibly record.
Second, we might record everything that can be recorded about the computation, in the hope that it might someday be useful. This also sounds straightforward but is surprisingly difficult to pin down, since “everything that can be recorded” can be interpreted in many different ways. Should we record every function call? Every instruction? Every molecular interaction? Do we need to record what the programmer had for breakfast on the day the program was written? Clearly we have to stop somewhere, and for efficiency reasons we should probably stop far short of any reasonable definition of “everything”.

Most extant approaches pick some intermediate point between these two extremes, committing to some (often not explicitly stated) choices about what is important about the computation that should be recorded in its provenance.

For example, in databases, there are models such as where-provenance [2] (tracking the “sources” of copied data), lineage [10], why-provenance [2] or how-provenance [14] (tracking tuples “used by” or that “justify” a result tuple), or dependency provenance [7] (a computable approximation of the information flow behavior of the program).

Provenance has also been studied extensively in other settings, particularly “scientific workflow” systems (e.g. [21, 20, 18]). Scientific workflows are usually high-level, visual programming languages, often based on dataflow or Petri-net models of concurrent computation, and often executed on grid or cloud computing platforms. This architecture has the advantage that it puts considerable computational power into the hands of scientists without forcing them to learn how to program parallel or distributed systems at a low level in C++ or Java. However, it also has a serious drawback: distributing a program over a heterogeneous network dramatically increases the number of things that can go wrong, typically makes the computation nondeterministic and makes it hard for the user to trust the results.

Scientists are reluctant to publish results based on programs that may contain subtle bugs, and whose behavior is different every time they are run, or depends on libraries or other environmental factors in subtle ways. Provenance is perceived as important for helping users understand whether results of such computations are repeatable and trustworthy, and in particular for scientists to be able to judge the scientific validity of results they may wish to publish.

The work on database provenance is distinctive in that several different formal models have now been defined for database query languages with well-understood semantics. This makes it easier to compare, relate and generalize these approaches, though such comparisons are only starting to appear [8, 14]. For most of these models, there are semantic guarantees (or even exact semantic characterizations) relating the provenance records to the denotation of the program. On the other hand, for workflow provenance, formal definitions of the meaning of workflow programs have only started to appear recently (see for example [29, 17]), while the provenance semantics of these tools is usually specified informally, at best [21]. As a result there is a confusing variety of models and styles of provenance for workflows.

To address this problem, there has been an ongoing community effort, centered on a series of “Provenance Challenges” [23], to understand and compare the qualitative behavior of these different systems and synthesize a common format for exchanging provenance among them. This effort has recently yielded a draft Open Provenance Model, or OPM [22]. Instances of this model are graphs whose nodes represent agents, processes or artifacts and whose edges represent dependence, generation or control relationships. The OPM has “semantics” in the sense of the Semantic Web, in that the nodes and edges are expected to have names that are meaningful to reasonably well-informed users. The OPM standard draws heavily on informal motivations such as “provenance is the process that led to a result” and “edges denote causal relationships linking the cause to the effect”. But while the OPM specifies a graph notation, controlled vocabulary for the edges, and inference rules for inferring new edges from existing edges, it
does not have a “semantics” in the denotational or operational sense by which we might judge whether a graph is consistent or complete or whether inferences on the graph are valid.

In this paper, we investigate the use of structural causal models [24] as a semantics for these graphs, and relate the informal motivations invoked in defining OPM graphs with the formal definitions of actual cause and explanation due to Halpern and Pearl [15,16]. We do not argue that structural causal models provide the only or best causal account of provenance. However, structural causal models are quite close to OPM-style provenance graphs (modulo cosmetic differences), so the analogy is compelling. Moreover, structural models have been studied extensively (e.g. [24,15,16,11,12,13]) and have proven useful to both philosophical accounts of scientific explanation [30] and psychological theories of understanding [27]. Nevertheless, it may be enlightening to apply other mathematical theories of causality and explanation to provenance, or investigate variations and extensions of Halpern and Pearl’s approach.

The broader aim of this paper is to argue by example that semantics (in the mathematical sense) is badly needed for research on provenance. One of the major motivations for provenance is to improve scientific communication, by allowing scientists to generate and exchange computational “explanations” or “justifications” of their results. In biology, for example, some journals now require both data and workflow programs describing how results were obtained, and some scientists anticipate that scientific publication will evolve into richer documents incorporating text, data, and computation [26]. However, if the techniques used to do so are poorly specified and unverified then we can expect errors and confusion. Programming languages and semantics researchers can and should be involved in making sure that these techniques are clearly described and robust, to help ensure that scientific communications retain long-term value as they gain computational structure.

2 Examples

Before delving into technical details, we give a high-level example comparing OPM-style provenance graphs with structural causal models.

The left-hand side of Figure 1 shows a simple OPM graph, based on a standard example showing the “provenance of a cake” [22]. The right-hand side shows a structural causal model, depicted as a graph. These two graphs are intentionally very similar. In the OPM graph, the ovals denote “artifacts” (flour, water, pan, cake) while the boxes denote “processes” (baking, mixing).

The OPM standard does not specify a semantics of provenance graphs as computations that might take place in the future; rather, it specifies a syntax for graphs that are supposed to describe processes that have taken place in the past. Nevertheless, it is natural to read an OPM graph as an expression or straight-line program that can be rerun to produce the output in the same way as the original process did.

Conversely, a causal model such as the one in Figure 1 does have an intended computational semantics. Each node in a causal model is equipped with a function specifying how to compute the value of the node given values for the parent nodes. An acyclic causal graph can be viewed as a piece of straight-line code, assigning values to variables as shown along the bottom of Figure 1. Here, we considered a simplistic boolean-valued model whose transfer functions are conjunctions. We can interpret these definitions as saying that if all of the needed ingredients for each step of the process are present, then that step will succeed.

Causal models also typically distinguish between the set of exogenous parameters $U$ and endogenous variables $V$. The former are meant to represent unknowns, measurement error, or environmental factors not otherwise taken into account in the model. Here, for example, we included one exogenous parameter
Mix := (Water ∧ Sugar ∧ Eggs ∧ Flour ∧ Butter) ⊕ U_1
Batter := Mix ⊕ U_2
Bake := (Batter ∧ Pan) ⊕ U_3
Cake := Bake ⊕ U_4

Figure 1: Top left: An OPM graph. Top right: the corresponding causal model. Bottom: a straight-line code description of both processes. Variables U_1, U_2, U_3, U_4 are exogenous variables (error terms, inputs) abstracting away unknown environmental influences that are not explicitly modeled.

U_i for each computation step, representing the possibility that something might go wrong.

Causal models are closely related to Bayesian networks, and causal models can also be given a probabilistic interpretation. For example, to model a scenario where the oven explodes and destroys the cake with probability 0.01, we can employ a probability distribution giving U_3 the expected value 0.01.

In artificial intelligence, probabilistic causal models are used either to represent domain knowledge that enables a system to reason about cause and effect, or as a representation of hypotheses about some data whose behavior is believed to be causal. Bayesian inference can then be used to learn causal models from data. This kind of inference is appropriate for data generated by controlled experiments where a single parameter can be varied to identify cause-effect relationships, but can also be used to analyze situations with less ideal experimental designs [24].

In this paper, however, we will consider only the deterministic form of causal models and focus on their use as a semantic tool, not on inference of causal models. We will show how to interpret a provenance graph as a causal model and relate syntactic and semantic techniques for reasoning about causality in provenance graphs.

3 Provenance Graphs

For the purposes of this paper, we will employ a simplified model of OPM-style provenance graphs, which we will just call provenance graphs. Fix a set of data values D, and a set of process names P. Recall that a bipartite graph \( G = (V,W,E) \) is a (here, directed) graph with vertices \( V \cup W \) and edges \( E \subseteq (V \times W) \cup (W \times V) \). A provenance graph is a bipartite graph in which the vertices are labeled. We call the vertices of \( V \) the artifacts and the call vertices of \( W \) the processes, and the artifact nodes are labeled with data values and the process nodes are labeled with process names. Intuitively, an edge
\((a,p) \in E\) means that \(a\) was generated by process \(p\), also written \(a\) was GeneratedBy \(p\), and an edge 
\((p,a) \in E\) means that \(a\) was used by process \(p\), also written \(p\) used \(a\).

We call a provenance graph functional if for each process node \(p \in W\) there is exactly one artifact \(a \in V\) such that \((p,a) \in E\). We also call a provenance graph sorted if there is a function \(ar : P \rightarrow \mathbb{N}\) such that each process node \(x\) has \(ar(x)\) inputs (with in-edges labeled \(1, \ldots, n\)). Note that a sorted functional provenance graph is essentially a first-order term with sharing, i.e. a first-order term with nonrecursive let-binding. However, for the purposes of this paper this sharing is important and it is more convenient to think in terms of graphs.

In this paper, we consider the simple case where provenance graphs are functional and both provenance graphs and causal graphs are acyclic. (Note that acyclic causal models are called “recursive” in the causal models literature.)

Now let us consider the provenance recording scenario described in the introduction: say we have some program that computes a function \(f : D^n \rightarrow D\) whose implementation is unknown. We assume a fixed set of artifact nodes \(V\) that includes at least \(n\) input nodes \(v_1, \ldots, v_n\) and a distinguished result node \(v_0\). A provenance graph semantics for \(f\) is a function \(Pf : D^n \rightarrow PG(V)\), where \(PG\) is the set of all provenance graphs over \(V\).

What properties should a provenance graph semantics have, beyond simply assigning each input a graph? We argue that there should be some relationship between the function \(f\) being described and the “meaning” of the provenance graph. But for this to be sensible, we first need to assign the graph a computational meaning.

Given a sorting \(ar\), an interpretation \([\cdot]\) associates each process name with a function \([p] : D^{ar(p)} \rightarrow D\). (Such an interpretation is essentially an algebra over the first-order signature \((P, ar)\).) Given a graph \(G\) with \(n\) input nodes \(v_1, \ldots, v_n\), we can therefore define a function \([G] : D^n \rightarrow D\) that takes a tuple of values for the input nodes, applies the interpretation functions to calculate the values for all of the nodes, and finally returns the value of the result node \(v_0\).

Given a provenance semantics \(Pf\) for an unknown function \(f\), we say that \(Pf\) is a pointwise approximation of \(f\) if for each input \(\vec{u}\), we have \([Pf(\vec{u})](\vec{u}) = f(\vec{u})\). In other words, we can recompute the value of \(f\) at \(\vec{u}\) directly using the provenance graph returned for \(\vec{u}\).

Most graph-based provenance semantics implicitly satisfy this property. But observe that there is always a trivial pointwise provenance semantics defined by taking \(Pf(\vec{u})\) to be a graph where the result node has no connection to the inputs and is labeled with \(f(\vec{u})\). This is a pointwise approximation, but gives us no insight into how the result depends on the inputs. Thus, capturing the original function pointwise is intuitively necessary, but not sufficient for the provenance graph to be informative. Something more is needed.

Given a provenance semantics \(Pf\) for \(f\), we say that \(Pf\) approximates \(f\) globally provided that for each \(\vec{u}\), we have \([Pf(\vec{u})] = f\). In other words, a global approximation yields a provenance graph that simulates \(f\) on all inputs. Note that a global approximation exists if (and only if) the language of provenance graphs is rich enough to express \(f\). Specifically, we define \(Pf\) as the constant function that returns a provenance graph that simply say “apply \(f\)”. Of course, if \(f\) is a large, opaque program then this may not be helpful.

The global criterion seems very strong: it requires the provenance graph to describe what would happen under an arbitrary change to the input, which may be far more information than we need to understand just one run of the program. Moreover, a global approximation semantics may not exist for reasonable combinations of provenance graph languages and semantics. For example, if the provenance graphs can make use of only arithmetic functions then we cannot globally approximate the behavior of a program that calculates a properly recursive function such as factorial — there is no fixed arithmetic circuit that calculates factorials. On the other hand, for certain simple classes of workflows, global
approximation is possible, and clearly desirable.

Instead of an all-or-nothing correctness property, we now consider the possibility of measuring how powerful a provenance semantics is as a way of predicting the function it is meant to represent.

Let \( P \) be a provenance semantics for \( f \). We define a relation on input tuples \( \vec{u} \) as follows:

\[
\vec{u} \rightsquigarrow \vec{u}' \iff [P \ f(\vec{u})](\vec{u}') = f(\vec{u}')
\]

In other words, \( \vec{u} \rightsquigarrow \vec{u}' \) holds just in case the provenance graph for \( f \) on \( \vec{u} \) correctly predicts the value of \( f \) on \( \vec{u}' \). That is, the relation \( \rightsquigarrow \) quantifies how the generality of the provenance graphs produced by \( f \).

We call the relation \( \rightsquigarrow \) the predictive power of provenance semantics \( P \).

Observe that \( \rightsquigarrow \) is reflexive if and only if \( P \) is pointwise approximation, and it is total if and only if \( P \) is a global approximation. Furthermore, given two provenance semantics \( P_1 \) and \( P_2 \), we can compare them by comparing their predictive power \( \rightsquigarrow_1 \) and \( \rightsquigarrow_2 \). Specifically, if \( \rightsquigarrow_1 \subseteq \rightsquigarrow_2 \) then \( P_2 \) has at least as much predictive power as \( P_1 \), which we might write formally as \( P_1 \leq P_2 \). Note that two provenance semantics might have equal predictive power but be very different as functions.

Given a language of provenance graphs and a fixed interpretation of the process names they may use, consider the problem of designing a provenance semantics for a given function \( f \) whose predictive power is as great as possible. Some interesting questions we will leave for future work include: Is there a unique “most powerful” semantics? Given the program text of \( f \), is there an effective way to produce the most powerful (or a reasonably good) semantics?

4 Causal models

In the discussion so far, the function \( f \) being investigated is essentially a black box — we can provide inputs and observe the output, and nothing else. There may be intermediate states and values calculated by \( f \) that are not visible externally, nor can we gain understanding of \( f \) by artificially altering intermediate states. Understanding can often be aided by considering hypothetical changes in the middle of a process. For example, suppose \( f \) is defined as follows:

\[
f(x, y, \vec{z}) = \frac{g(\vec{z})}{(x^2 - 1)y}
\]

Then \( f(1, 0, \vec{z}) \) is undefined (division by zero), but there is no way to change just one input variable to a value such that \( f \) is defined. Of course, inspecting the definition of the function makes it obvious that both \( x \) and \( y \) need to change, but if \( f \) is a black box and \( x \) and \( y \) are just two of many input parameters then finding a way to change the inputs to fix the problem would require many blind guesses. If we could see inside of \( f \) and possibly change some intermediate error results to dummy valid results, then we might be able to find the problem more easily.

Structural causal models are (from a certain point of view) models of computation that permit some inspection and intervention upon the intermediate results. We will now review standard definitions of causal models and actual causes from [15, 16].

A causal model \( M = (U, V, F) \) is a structure where \( U \) is a set of inputs (or exogenous variables), \( V \) is a set of (endogenous) variables, and \( F \) is a family of functions \( F_X : (D^U \rightarrow D) \) mapping each vertex \( X \) in \( V \) to a function from tuples of data values to data values indexed by \( V \). A causal graph \( G = (U \cup V, E) \) for \( M \) is a directed graph whose vertices are inputs or events of \( M \) and such that \( F_X \) depends only on the values corresponding to parent vertices of \( X \) in \( G \). We restrict attention to causal models whose underlying graph is acyclic (these are sometimes called “recursive” models in the structural-models.
literature). For each acyclic causal model there is a unique least causal graph expressing all and only the true dependencies of the functions $F_X$.

A valuation is simply a $V$-indexed tuple of values in $D$, or $\sigma : D^V$. We say a valuation is consistent if for each $X$ we have $F(X)(\sigma) = \sigma(X)$. A causal model paired up with a (consistent) valuation is called a (consistent) causal situation.

Interventions are a distinctive feature of causal models. Given a model $M$, we can form another models $M_{[X := x]}$ by fixing the value of vertex $X$ to $x$ and making the value of $X$ independent of its former inputs. This reflects the fact that although the causal model represents the behavior of a closed system, we can reach into the system (at least as a thought experiment) and change $X$ to a value of our choice.

**Definition 1.** If $M = (V, U, F)$ is a causal model, then the result of setting $X$ to $x$ in $M$ is $M_{[X := x]} = (V, U, F')$, where:

$$F'_Y(\sigma) = \begin{cases} x & |X = Y \\ F_Y(\sigma) & |X \neq Y \end{cases}$$

If the appropriate variable $X$ is clear from context, this may be written $M_x$.

We also review Halpern and Pearl’s definition of “actual cause”.

**Definition 2 (Actual cause).** Let $(M, \sigma)$ be a causal situation. Let $\bar{X}$ be a subset of $V$ and $Y \in V$, and suppose $\bar{x} = \sigma(\bar{X})$ and $y = \sigma(Y)$. Suppose that:

1. $\sigma(\bar{X}) = \bar{x}$ and $\sigma(Y) = y$.
2. Some set of variables $W \subseteq V - X$ and values $\bar{w} \in D$, and $\bar{w}' \in D$ exist such that:
   
   (a) $Y \neq y$ holds in $M_{\bar{x}, \bar{w}}$
   
   (b) $Y = y$ holds in $M_{\bar{x}, \bar{w}', \bar{z}}$ for all $Z \subseteq V - (X \cup W)$, where $\bar{z}$ are the values of $\bar{Z}$ in $M$.

Then we say that $\bar{X} = \bar{x}$ is an weak cause of $Y = y$. Moreover, if no proper subset of $\bar{X} = \bar{x}$ is a weak cause, then $\bar{X} = \bar{x}$ is an actual cause of $Y = y$.

The definition of actual cause deserves explanation. Briefly, the idea is that an actual cause must first describe the true state of affairs (part 1). Secondly, there must be a way to change the value of $Y$ by changing the values of $X$ (possibly plus some other variables $W$), and there must not be a way of changing the value of $Y$ by fixing the values of $X = \bar{x}$, $W = \bar{w}'$ and setting any other variables to their original values. (In fact, the variables $Z$ are usually between $X$ and $Y$.)

For additional discussion we must refer the reader to Halpern and Pearl [15]. The discussion of actual causes later in this paper does not depend heavily on the details of this definition.

## 5 Causal interpretations of provenance graphs

Given a fixed interpretation of the process identifiers of a provenance graph $G = (V, W, E)$, we can define a causal model and a valuation $(M_G, \sigma_G)$. Suppose $V = U' \uplus V'$ where $U'$ is the set of input nodes in $G$ (that is, artifact nodes not generated by any process). Let $M_G = (U', V' \cup W, F)$, where we define $F_v(\sigma)$ for $v \in V'$ as the (unique) value of $\sigma(p)$ where $p$ is the process node that generates $v'$, and $F_p(\sigma)$ is the interpretation function for node $p$ in $G$, lifted to apply to $\sigma$ by ignoring all values of nodes not used by $p$ in $\sigma$. Moreover, we define the valuation $\sigma_G$ for $M_G$ by taking $\sigma_G(v)$ to be the data value assigned to $v$ in $G$.

Just as the functional interpretation of a provenance graph can be viewed as a local approximation of some unknown (functional) process, its causal model interpretation can be viewed as an approximation
of some unknown (causal) process. To make this idea precise, we introduce an abstract notion of “causal functions” that support both ordinary evaluation and intervention.

A causal function over variables \((U,V)\) is a family of functions \(f_\tau : D^U \to D^V\), one for each partial valuation \(\tau : V \to D\). We write \(f\) for \(f_{\emptyset}\), and we require that for each partial valuation \(\tau\) and input valuation \(\sigma\) we have \(\tau \subseteq f_\tau(\sigma)\). Thus, for example, \(f(\sigma)\) computes all of the values of variables directly from the inputs without any interference, while \(f_{[X:=x;Y:=y]}(\sigma)\) calculates the values when \(X\) is forced to be \(x\) and \(Y\) is forced to be \(y\). Note that a causal model \(M\) defines a unique causal function, which we will write \([M]\). On the other hand, the definition of causal function makes sense without talking about the specific propagation mechanism used to calculate the values.

Suppose that \(f\) is a causal function with inputs \(U\) and variables \(V\), and let \(Pf\) be a function mapping input values \(\vec{u} \in D^U\) to causal models \(Pf(\vec{u})\) over inputs \(U\) and variables \(V\). Then \([Pf(\vec{u})]\) is again a causal function for each \(\vec{u}\).

We say that a provenance semantics \(P\) approximates \(f\) pointwise if for any \(\vec{u}\), we have \([Pf(\vec{u})](\vec{u}) = f(\vec{u})\). That is, both the end results and intermediate states of \(Pf\) agree with \(f\). As with pointwise approximations in the functional case, this is a rather weak specification, since it is satisfied by defining \(Pf(\vec{u})\) as a disconnected causal process that simply defines each variable \(X \in V\) to be a constant \(f(\vec{u})(X)\).

Likewise, we can define \(Pf\) to be a global approximation of \(f\) when \([Pf(\vec{u})]{\vec{u}} = f\) for any \(\vec{u}\). Again, this is very strong, since it says that \(f\) must be expressible as a single causal model — that is, the provenance graph for \(f\) tells us everything about the causal structure of \(f\).

Casual functions admit a third natural notion of approximation, which is strictly in between pointwise and global approximation. We say that provenance semantics \(Pf\) approximates \(f\) locally if for any \(\vec{u}\), we have

\[
[Pf(\vec{u})]_{\vec{u}}(\vec{u}) = f_\tau(\vec{u})
\]

That is, approximating \(f\) locally does not require that showing how \(f\) would behave on arbitrary inputs, but does ensure that we can predict how the particular run of \(f(\vec{u})\) would change if we had intervened by fixing the values of the variables in \(V\).

Local approximation is strictly stronger than pointwise approximation: clearly local implies pointwise, but for a simple process such as \(Y := X + 1; Z := Y \times 2\) the trivial pointwise approximation is not a local approximation. The requirement to handle arbitrary interventions forces us to do more than simply record the actual values of the intermediate variables; instead, we must record at least some information about how they were related.

On the other hand, global approximation obviously implies local approximation, but not the converse. Local approximation is strictly weaker than global approximation, since there is no requirement that the causal model obtained for a run on input \(\vec{u}\) will be useful for predicting results or causal structure of \(f\) running on another input. This allows different causal models to be used for different inputs, as long as the causal structure of the model chosen for \(f\) only depends on depend on the input parameters, not intermediate variable values.

For example, consider \(f(u;x,y) = (x+y)^u\), where the provenance graph may only employ multiplication and addition. Then there is no single provenance graph that approximated \(f\) globally, but for each choice of \(u\) there is a graph that describes the causal function \(x,y \mapsto f(u;x,y)\).

As with the functional case, we might also expect a causal model to have partial explanatory power for other input settings. Specifically, we define the predictive power of \(Pf\) as the relation:

\[
\vec{u} \sim \vec{u}' \iff \forall \tau. [Pf(\vec{u})]_{\vec{u}}(\vec{u}') = f_\tau(\vec{u}')
\]

In other words, \(\vec{u} \sim \vec{u}'\) holds when the causal model generated from the provenance of \(\vec{u}\) is a faithful model of the behavior of \(f\) at \(\vec{u}'\) under arbitrary interventions.
For this definition of predictive power, local and global approximation correspond to reflexivity and totality of $\rightarrow$. As with the functional case, we can compare provenance semantics by their predictive power.

6 Inferences about causality in provenance

The OPM standard also describes inferences on provenance graphs. These inferences are formalized as Datalog-style inference rules that allow us to infer new edges from existing edges. For our provenance graphs, the relevant rules from the OPM standard include:

\[
\begin{align*}
  x \text{ wasDerivedFrom } y & :\leftarrow x \text{ wasGeneratedBy } p \land p \text{ used } y \\
  p \text{ wasTriggeredBy } q & :\leftarrow p \text{ used } x \land x \text{ wasGeneratedBy } q \\
  x \text{ wasDerivedFrom}^+ y & :\leftarrow x \text{ wasDerivedFrom } y \lor (x \text{ wasDerivedFrom } z \land z \text{ wasDerivedFrom}^+ y) \\
  p \text{ wasTriggeredBy}^+ q & :\leftarrow p \text{ wasTriggeredBy } q \lor (p \text{ wasTriggeredBy } r \land r \text{ wasTriggeredBy}^+ q)
\end{align*}
\]

For example, if process $p$ “used” artifact $x$ which “was generated by” process $q$, then we infer that $p$ “was triggered by” $q$. However it is important to note that the terms “used”, “was generated by” and “influenced” are simply different edge labels whose relationship is being axiomatized by the Datalog rules — there is no connection in the standard to the causal-model interpretation of provenance graphs which we have introduced in this paper.

We want to give these edge relations meaning in terms of the causal model interpretation, and use this as a basis for judging the correctness of inferences. In particular, we would like the edges to correspond to causal relationships, as they are expected to do in OPM.

Consider a naive interpretation in which we interpret $p \text{ used } x$ as meaning that $x = \sigma(x)$ was part of an actual cause of $p = \sigma(p)$ in $M_G$, and likewise interpret $x \text{ wasGeneratedBy } p$ as meaning that $p = \sigma(p)$ was part of a actual cause of $x = \sigma(x)$ in $M_G$. However, this is a little too naive, since it is possible for $X = x$ to actually cause $Y = y$ and $Y = y$ to actually cause $Z = z$, while in OPM graphs, the used and wasGeneratedBy edges should not have this behavior. We can fix this by further constraining these relations to hold only when there is no other actual cause “between” $p$ and $x$. Using these definitions of the basic edges, we can extrapolate meanings for the other edges using the Datalog rules: for example, $x \text{ wasDerivedFrom } y$ means that $Y = y$ is part of an actual cause of $X = x$ and there is no other artifact strictly between $x$ and $y$, and wasDerivedFrom$^+$ is the transitive closure, which (for a finite causal model) is equivalent to saying that $Y = y$ is part of an actual cause of $X = x$ without any constraints. (We leave these observations as conjectures for now.)

However, there is an important problem with the above situation: namely, we have defined the meanings of the edges in terms of the definition of actual cause, not in terms of the presence or absence of edges in $M$. Although every actual cause relationship corresponds to an edge, there may also be edges that are syntactically present in $M_G$ but do not correspond to immediate actual causes. The possible flows of information exhibited by the causal model do not always correspond to actual causes. In other words, the Datalog rules are complete, but unsound, with respect to actual causality; the naive approach of simply following all syntactic links to find all nodes reachable from a given node is a safe over-approximation (but it may be very inaccurate).

To clarify this point, we review some of the complexity results of Eiter and Lukasiewicz [11]. For deterministic causal models, they study the complexity of several definitions of causality, including the “actual cause” definition introduced by Halpern and Pearl [15]. They show that determining whether
a set of variables and values is an actual cause of another event is NP-hard, even for Boolean causal models. These complexity lower bounds hold whether or not the function definitions are considered part of the problem, since in the Boolean case the amount of information needed to describe the operators is small. Datalog queries can be computed in polynomial time [19], so cannot in general correctly calculate actual causes.

7 Related and future work

As discussed in the introduction, we draw on previous work on causality based on structural models in artificial intelligence (see for example [24] for a comprehensive discussion of this work and its applications). The worst-case complexity and special cases of computing actual causes and causal explanations is comprehensively studied by a series of papers by Eiter and Lucasiewicz [11, 12, 13]. As we have noted, these have immediate applications to showing that simple transitive closure algorithms for extracting actual causes from provenance cannot suffice for provenance inference, at least if Halpern and Pearl’s definitions are used.

Halpern gave a well-received invited presentation on causality, responsibility and blame at a recent workshop on provenance [5]. The analogy between causal models and provenance has been “in the air” since then, and has been discussed in more recent work by Chapman et al. [4] and an overview paper by Cheney et al. [9].

The treatment of causality here plays a similar role to dependence in previous work with Acar and Ahmed on dependency provenance [7], and subsequently on a “complete provenance trace” model [6]. These models support some inference concerning how hypothetical changes to (parts of) the input affect (parts of) the output. However, these techniques are based on a database query language supporting arbitrarily nested sets and records, which do not seem to match structural causal models over atomic data. Acar et al. [1] presents a translation from a core database query language to OPM-style provenance graphs; the graphs in that work do not have a causal or computational interpretation, but exploring this possibility is an obvious next step.

In this paper, we have focused on a (perhaps deceptively) simple setting where the provenance graphs are directly analogous to causal models. It is not clear how far this analogy can be pushed using known forms of causal models; it is possible that extensions to the causal framework are needed to provide semantics for provenance models describing richer computational models. For example, matters likely become more interesting in the presence of concurrent processes that may interact with one another (see for example [28]). This is a common case in scientific workflow provenance and causal provenance semantics should be developed for (or adapted to) models such as dataflow networks or process.

There are several other developments in structural causal models that would be interesting to explore from the point of view of provenance, including using probabilistic causal models to explain how provenance can make unreliable computations statistically “repeatable”, and using existing definitions of explanation, responsibility and blame for provenance.

Finally, as illustrated by the “cake” example, provenance records sometimes employ an implicit notion of state and resource consumption. For example, in baking a cake, some inputs are “consumed” (e.g. the ingredients), while others are only catalysts (e.g. the cake pan). The provenance model also does not reflect time or resource usage. Of course, this kind of information can be added to the data model (and the OPM draft already allows for both time and domain-specific annotations), but it would be interesting to explore applications of linear or resource-sensitive logics to this setting.
8 Conclusions

We have explored an analogy between the OPM-style provenance graphs that are becoming popular in scientific workflow systems (and other settings) and structural causal models as developed by Pearl, Halpern and others in artificial intelligence. In particular, a provenance graph can be interpreted as a causal model in a natural way, provided that we know how to interpret the processing steps as functions. We considered the problem of using provenance graphs to represent particular runs of a program. Existing definitions and results concerning causal models can be lifted to provenance graphs.

We also investigated the problem of inferring actual causes over provenance graphs using Datalog-style rules. As shown by the complexity of computing or calculating explanations in the Halpern-Pearl approach is quite high (usually at least NP-hard), which shows that, for example, queries about actual cause or explanation cannot be expressed using Datalog rules, even in the special case of provenance graphs over Boolean functions. This shows that Halpern and Pearl’s definitions of actual cause and the ad hoc rules that have been proposed for reasoning about provenance graphs are incompatible.

These observations are not deep — they amount to applying known results in the structural causality literature to analyze informal claims in the provenance literature. Adopting a different model of causality might lead to different conclusions. Nevertheless, we believe that the exercise of trying to formalize the relationship between provenance and causal explanation has not been seriously tried before and is worthwhile, if for no other reason than to provoke others to do a better job.

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