Constraining the Nuclear Equation of State via Gravitational-wave Radiation of Short Gamma-Ray Burst Remnants

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Abstract

The observed internal plateau of X-ray emission in some short gamma-ray bursts (GRBs) suggests the formation of a remnant supramassive magnetar following a double neutron star (NS) merger. In this paper, we assume that the rotational energy is lost mainly via gravitational-wave radiation instead of magnetic dipole (MD) radiation, and present further constraints on the NS nuclear equation of state (EoS) via mass quadrupole deformation and \( r \)-mode fluid oscillations of the magnetar. We present two short GRBs with measured redshifts, 101219A and 160821B, whose X-ray light curves exhibit an internal plateau. This suggests that a supramassive NS may survive as the central engine. By considering 12 NS EoSs, within the mass quadrupole deformation scenario we find that the GM1, DD2, and DDME2 models give an \( M_p \) band falling within the 2\( \sigma \) region of the proto-magnetar mass distribution for \( \varepsilon = 0.01 \). This is consistent with the constraints from the MD radiation dominated model of rotational energy loss. However, for an \( r \)-mode fluid oscillation model with \( \alpha = 0.1 \) the data suggest that the NS EOS is close to the Shen and APR models, which is obviously different from the MD radiation dominated and mass quadrupole deformation cases.

Unified Astronomy Thesaurus concepts: Gamma-ray bursts (629); Gravitational waves (678)

1. Introduction

One favored progenitor model for short gamma-ray bursts (GRBs) is the coalescence of two neutron stars (NS–NS; Paczynski 1986; Eichler et al. 1989). On 2017 August 17, the first direct detection of gravitational waves (GWs; GW170817) and an electromagnetic counterpart originating from the merger of a binary NS system was achieved via the collaboration of Advanced LIGO, Advanced VIRGO, Fermi, as well as optical telescopes (Abbott et al. 2017a, 2017b; Covino et al. 2017; Goldstein et al. 2017; Kasen et al. 2017; Savchenko et al. 2017; Zhang et al. 2018). The near-coincident detection of a short GRB potentially provides the first “smoking gun” evidence that at least some short GRBs originate from NS mergers.

The remnant of double NS mergers remains an open question, and is dependent on the total mass of the post-merger system and the poorly known NS equation of state (EoS; Lasky et al. 2014; Li et al. 2016). One possible remnant of such mergers is a supramassive NS, which may survive for seconds to hours before collapsing into a black hole (BH) if the nascent NS mass is less than the maximum gravitational mass (Hotokezaka et al. 2013; Zhang 2014; Lü et al. 2015; Foucart et al. 2016; Gao et al. 2016; Kiuchi et al. 2018). Observationally, a good fraction of the X-ray light curves of short GRBs were discovered to show an extended plateau, a nearly flat light curve extending to hundreds of seconds, followed by a sharp decay with a decay index \( r^{-8.9} \) (called internal plateau; Rowlinson et al. 2010, 2013; Lü et al. 2015). Such a feature is very difficult to explain if it is powered by a BH engine, but seems to be consistent with the prediction of a rapidly spinning, supramassive NS (also called a millisecond magnetar). The sharp decay following the X-ray plateau is interpreted as the supramassive NS collapsing into a BH after it spins down due to magnetic dipole (MD) or GW radiation (Usov 1992; Thompson 1994; Dai & Lu 1998a, 1998b; Zhang & Mészáros 2001; Dai et al. 2006; Gao & Fan 2006; Metzger et al. 2008; Fan et al. 2013; Zhang 2013, 2014; Ravi & Lasky 2014; Lü et al. 2015, 2017; Gao et al. 2016; Chen et al. 2017).

Previous studies have shown that the newly born supramassive magnetar collapsing into a BH is triggered by the loss of a large amount of rotational energy due to MD radiation, and have estimated the physical parameters (i.e., the initial rotation period \( P_0 \) and the strength of the dipole magnetic field \( B_0 \)) and constrained the NS EoS (Rowlinson et al. 2010, 2013; Lasky et al. 2014; Lü et al. 2015). However, they found that the inferred initial rotation period is much longer than that expected in the double NS merger model (Friedman et al. 1986; Rowlinson et al. 2013; Lü et al. 2015). Such a puzzle might be solved in two ways. One is a low efficiency conversion of the magnetar wind energy into radiation, but it seems to be less likely given the higher expected efficiency of magnetic energy dissipation processes (Drenkhahn & Spruit 2002; Xiao & Dai 2019), or the varying gravitational mass and baryonic mass of the NS (Gao et al. 2019). The other solution is that most of the rotational energy of the magnetar was carried away via strong GW wave radiation (Fan et al. 2013; Lasky et al. 2014). If this is the case, the GW radiation of a newly born magnetar can be produced via either a mass quadrupole deformation with ellipticity \( \varepsilon \) for an NS rotating as a rigid body or an \( r \)-mode fluid oscillation with amplitude \( \alpha \) (Owen et al. 1998; Lindblom et al. 1998; Andersson & Kokkotas 2001; Zhang & Mészáros 2001; Owen 2010; Yu et al. 2010; Fan et al. 2013; Lasky 2015; Ho 2016; Lasky & Glampedakis 2016; Lü et al. 2017). These GW signals are too weak to be detected by the current Advanced LIGO and Advanced Virgo observatories (Alford &
Schwenzer 2014, 2015; Abbott et al. 2017c; Lü et al. 2017; Ai et al. 2018).

One interesting question is: can a magnetar’s rotational energy loss dominated by GW radiation be used to constrain the NS EoS? In this paper, by analyzing the X-ray emission of short GRBs 101219A and 160821B, we used the observed data to constrain the EoS of NSs, and then compared the constraints of a mass quadrupole deformation for different \( \varepsilon \) with an r-mode fluid oscillation for different \( \alpha \). This paper is organized as follows. The GW radiation constraints on the NS EoS are presented in Section 2. In Section 3, we show the results of the constraints for GRBs 101219A and 160821B. The conclusions are drawn in Section 4 with some discussions. Throughout the paper, a concordance cosmology with parameters \( H_0 = 71 \text{ km s}^{-1} \text{ Mpc}^{-1} \), \( \Omega_M = 0.30 \), and \( \Omega_{\Lambda} = 0.70 \) are adopted.

2. Constraining the NS EoS via GW Radiation Dominated Rotational Energy Losses

The rapid decay after the X-ray plateau in the afterglow of short GRBs indicates that the supramassive NS is collapsing into a BH. If this is the case, the inferred collapse time can be used to constrain the NS EoS (Lasky et al. 2014; Ravi & Lasky 2014; Lü et al. 2015). In this section, we further constrain the NS EoS by assuming that the loss of rotational energy of the newly born magnetar is dominated by GW radiation. We will discuss two different scenarios of GW radiation as follows.

2.1. GW Radiation from Mass Quadrupole Deformation

The energy reservoir of a millisecond magnetar is the total rotation energy of the NS in rigid rotation, and it is written as

\[
E_{\text{rot}} = \frac{1}{2} I \Omega^2 \simeq 2 \times 10^{42} \text{ erg} \, M_{1.4} R_{6}^2 P_{-3}^2,
\]

where \( I, \Omega, P, R, \) and \( M \) are the moment of inertia, angular frequency, rotating period, radius, and mass of the NS, respectively. The convention \( Q = 10^7 Q_s \) in cgs units is adopted. A magnetar loses its rotational energy in two ways: MD torques \( (E_{\text{em}}) \) and GW radiation \( (E_{\text{gw}, q}) \),

\[
E_{\text{rot}} = I \Omega \dot{\Omega} = E_{\text{em}} + E_{\text{gw}, q} = -\beta I \Omega^4 - \gamma_q I \Omega^6 ,
\]

where \( \Omega \) is the time derivative of the angular frequency, \( \beta = \eta B_p^2 R_6^8 / 6 c^7 I \), and \( \gamma_q = 32 G \varepsilon^2 / 5c^5 \). \( B_p \) is the surface magnetic field at the pole, \( \varepsilon = (I_{xx} - I_{yy})/(I_{xx} + I_{yy}) \) is the ellipticity in terms of the principal moment of inertia, and \( \eta \) is the efficiency of converting the magnetar wind energy into X-ray radiation.

If the magnetar loses most of its rotational energy via GW radiation, one has

\[
E_{\text{rot}} = I \Omega \dot{\Omega} \simeq -\gamma_q I \Omega^6 .
\]

The full solution of \( P = 2 \pi / \Omega \) in Equation (3) can be written as

\[
P(t) = P_0 \left( 1 + \frac{2048 \pi^4 G \varepsilon^2}{5 c^5 P_0^6} \right)^{1/4}
= P_0 \left( 1 + \frac{2t}{\tau_{gw,q}} \right)^{1/4} ,
\]

where \( P_0 \) is the initial period at \( t = 0 \) and \( \tau_{gw,q} \) is characteristic spin-down timescale in this scenario. Following Ho (2016), \( \tau_{gw,q} \) can be given as

\[
\tau_{gw,q} = \left| \frac{E_{\text{rot}}}{E_{\text{gw}, q}} \right|_0 = \frac{1}{2 \eta \Omega_0^2} \left| \frac{D_4}{\varepsilon_3} \right|^{2/3} P_0^{-4/3}.
\]

Based on Equation (5), one can derive the initial period of the magnetar \( P_0 \),

\[
P_{0,3} = 0.1 \times (D_4^{14} \varepsilon_3^{-1/3} \tau_{gw,q}^{1/3})^{-1/3}.
\]

For a given EoS, the maximum gravitational mass \( (M_{\text{max}}) \) depends on the period and the maximum NS mass for a non-rotating NS \( (M_{\text{TOV}}) \). It can be expressed as (Lyford et al. 2003; Lasky et al. 2014)

\[
M_{\text{max}} = M_{\text{TOV}} (1 + \dot{\alpha} P^\beta),
\]

where \( \dot{\alpha} \) and \( \dot{\beta} \) depend on the NS EoS. The values of \( \dot{\alpha} \) and \( \dot{\beta} \) for given EoSs are presented in Table 1.

As the NS spins down, the maximum mass \( M_{\text{max}} \) gradually decreases. When the proto-magnetar mass \( (M_p) \) is close to \( M_{\text{max}} \), the centrifugal force can no longer sustain the gravitational force and the NS will collapse into a BH. By adopting Equations (4) and (7), one can derive the collapse
time \( t_{\text{col}} \) as a function of \( M_p \) in this scenario:

\[
t_{\text{col}} = \frac{5}{2048\pi^2 G \varepsilon^2} \left[ \frac{M_p - M_{\text{TOV}}}{\alpha M_{\text{TOV}}} \right]^{4/3} \cdot P_0^4
\]

and the full solution of \( \tau_{\text{gw},r} \) is known. \( P_0 \) and \( t_{\text{col}} \) can be inferred from the X-ray observations of short GRBs (more details will be discussed in Section 4). Moreover, the Galactic binary NS population has a high mass distribution with \( M_p = 2.46^{+0.13}_{-0.10} M_\odot \) (Valentini et al. 2011; Kiziltan et al. 2013). Here, we assume that the distribution of cosmological binary NS masses is the same as that of Galactic binary NS systems.

2.2. GW Radiation from \( r \)-mode Fluid Oscillation

In the above discussion, it is assumed that the NS undergoes rigid rotation. However, the NS may be treated as a fluid instead of a rigid body. If this is the case, the dominant GW radiation source of a newly born magnetar should be the unstable \( r \)-mode fluid oscillations with amplitude \( \alpha \), whose restoring force is the Coriolis force (Haskell et al. 2015; Lasky 2015). Actually, GW radiation via the \( r \)-mode instability of a rotating NS had been discussed in the early days (Chandrasekhar 1970; Friedman & Schutz 1978; Andersson 1998; Friedman & Morsink 1998; Strohmayer & Mahmoodyifar 2014). The spin-down of a newly born NS can be caused by an \( r \)-mode instability with an oscillating amplitude because of the loss of its angular momentum (Lindblom et al. 1998; Owen et al. 1998).

Within this scenario, the newly born magnetar spinning down loses its rotational energy via the MD and \( r \)-mode GW (\( \dot{E}_{\text{gw},r} \)) radiation (Owen et al. 1998; Andersson & Kokkotas 2001; Owen 2010; Ho 2016)

\[
\dot{E}_{\text{tot}} = I \Omega \dot{\Omega} = \dot{E}_{\text{em}} + \dot{E}_{\text{gw},r} = -\beta I \Omega^5 - \gamma I \Omega^8,
\]

where \( \gamma = (96\pi/15^2)(4/3)^6 (GMR^4J^2/c^7\Omega)^2 \alpha^2 \), \( I = 1/MR^2 \) and \( \beta \) are dimensionless. Following Alford & Schwenzer (2014) and Ho (2016), we adopt the constant values of \( J = 0.0205 \) and \( I = 0.3 \) in our calculations.

If the NS spins down by losing its rotational energy via GW radiation dominated by the \( r \)-mode, one has

\[
\dot{E}_{\text{rot}} = I \Omega \dot{\Omega} \simeq -\gamma I \Omega^8,
\]

and the full solution of \( P(t) \) in Equation (10) can be written as

\[
P(t) = P_0 \left[ 1 + \frac{\pi^7}{25} \left( \frac{16}{3} \right) \left( \frac{GMR^4J^2}{c^7\Omega^2} I \right) \right]^{1/6}
\]

\[
P(t) = P_0 \left[ 1 + \frac{3t}{\tau_{\text{gw},r}} \right]^{1/6},
\]

where \( \tau_{\text{gw},r} \) is the characteristic spin-down timescale in the \( r \)-mode scenario; \( \tau_{\text{gw},r} \) can be given by (Ho 2016)

\[
\tau_{\text{gw},r} = \left( \frac{E_{\text{tot}}}{\dot{E}_{\text{gw},r}} \right)^{1/2} = \frac{1}{2} \frac{1}{2 \gamma I \Omega^8}
\]

\[
= 4.3 \times 10^5 \text{s} \omega^{-7/4} P_0^{4/3}. \tag{12}
\]

Based on Equation (12), one can derive the collapse time \( t_{\text{col}} \) as a function of \( M_p \) in this scenario

\[
t_{\text{col}} = \frac{25}{\pi^7} \left( \frac{3}{16} \right) \left( \frac{GMR^4J^2}{c^7\Omega^2} \right) \left( \frac{M_p - M_{\text{TOV}}}{\alpha M_{\text{TOV}}} \right)^{6/3} \cdot P_0^5
\]

\[
= \frac{\tau_{\text{gw},r}}{3P_0^6} \left( \frac{M_p - M_{\text{TOV}}}{\alpha M_{\text{TOV}}} \right)^{6/3} - P_0^5. \tag{14}
\]

Similar to Equation (8), \( M_{\text{TOV}}, \alpha \), and \( \beta \) are known for a given NS EoS, and \( P_0 \) and \( \tau_{\text{gw},r} \) can be inferred from the observations.

3. Constraining the NS EoS from the Observations of Short GRBs 101219A and 160821B

The observed internal plateau of X-ray emission in short GRBs suggests that the central engine of at least some short GRBs are supramassive NSs (Rowlinson et al. 2010). Here we selected two short GRBs, 101219A and 160821B, whose X-ray emissions exhibit an internal plateau feature and have a measured redshift (Fong et al. 2013; Rowlinson et al. 2013; Lü et al. 2017). Our purpose is to further constrain the NS EoS by considering GW radiation dominated (mass quadrupole deformation and \( r \)-mode fluid oscillation) magnetar energy loss via these two short GRBs.

3.1. Observations and Light-curve Fits

The GRB 101219A, triggered by Swift/Burst Alert Telescope (BAT), is defined as a short GRB with \( T_0(15-350 \text{ keV}) = 0.6 \pm 0.2 \text{ s} \) (Gelbord et al. 2010; Krimm et al. 2010), and a redshift of \( z = 0.718 \) (Chomack & Berger 2011). The Swift/X-Ray Telescope (XRT) began observation of the GRB field 61s after the BAT trigger (Golenetskii et al. 2010). The X-ray afterglow of this GRB presents a plateau emission, followed by a steep decay. More details of the X-ray light curve are given in Evans et al. (2007, 2009). A smooth broken power-law function is adopted to fit the X-ray light curve

\[
F = F_0 \left[ \frac{t}{t_b} \right]^{-\alpha_1} + \left[ \frac{t}{t_b} \right]^{-\alpha_2} \right]^{-1/\omega}, \tag{15}
\]

where \( \omega \) describes the sharpness of the break and is taken to be 3 in this analysis (Liang et al. 2007). One has \( \alpha_1 = -0.01 \pm 0.09 \), \( \alpha_2 = -17.32 \pm 16.79 \), and the break time \( t_b = 203 \pm 22 \text{ s} \) (see Figure 1).

GRB 160821B is a nearby short GRB with a redshift of \( z = 0.16 \) (Levan et al. 2016), and was triggered by Swift/BAT with \( T_0(15-350 \text{ keV}) = 0.48 \pm 0.07 \text{ s} \) (Palmer et al. 2016; Lü et al. 2017). The XRT began observation of the GRB field
57 s after the BAT trigger (Siegel et al. 2016), and its X-ray light curve is also characterized by a nearly flat \( \alpha_1 = -0.36 \pm 0.05 \) plateau extending to \( t_b = 176 \pm 3 \) seconds, followed by a rapid decay with \( \alpha_2 = -4.47 \pm 0.23 \) (Figure 1).

### 3.2. Constraining the EoS

If the rotational energy is lost mainly via GW radiation, one has roughly \( t_{col} = t_b/(1 + z) \), where \( t_{col} \) is the smaller value between \( \tau_{gw,\theta} \) and \( \tau_{gw,r} \). One can then derive the lower limit of \( P_0 \) in the mass quadrupole deformation and \( r \)-mode fluid oscillation channels. The only remaining variables in Equations (8) and (14) are related to the NS EoS. Here, we consider 12 EoSs that are usually discussed in the literatures (see Table 1), and EoS parameters are taken from Lasky et al. (2014), Ravi & Lasky (2014), Li et al. (2016), and Ai et al. (2018).

Figures 2 and 3 show the \( t_{col} \) as a function of proto-magnetar mass \( (M_p) \) for GRB 101219A and GRB 160821B, respectively. Different colored lines correspond to different EoSs. The gray shaded region is the proto-magnetar mass distribution that is derived independently from the binary NS mass distribution in our Milky Way (Kiziltan et al. 2013; Lasky et al. 2014), and the horizontal dashed lines are the observed collapse time for the GRBs 101219A and 160821B.

Within the scenario where the GWs are produced by mass quadrupole deformation, the ellipticity \( \varepsilon \) is required to be as large as 0.01 if the rotational energy is lost mainly via GW radiation (Fan et al. 2013; Lasky et al. 2014; Ho 2016). As such, we adopt \( \varepsilon = 0.01 \) in our calculations. We find that the GM1, DD2, and DDME2 models give an \( M_p \) band falling within the 2\( \sigma \) region of the proto-magnetar mass distribution in both GRBs 101219A and 160821B (see Figure 2). The correct EoS should be close to those three models, wherein the maximum mass for a non-rotating magnetar is \( M_{TOV} = 2.37 M_\odot, 2.42 M_\odot, \) and \( 2.48 M_\odot \), respectively.
Alternatively, if the GWs are produced by the \( r \)-mode fluid oscillation and dominate the energy loss, the \( r \)-mode amplitude \( \alpha \) is required to be as large as 0.1 (Ho 2016). By adopting \( \alpha = 0.1 \) in our calculations, we find that the Shen and APR models give an \( M_p \) band falling within the 2\( \sigma \) region of the proto-magnetar mass distribution in both GRBs 101219A and 160821B (see Figure 3). The maximum masses for a non-rotating magnetar in these two models are \( M_{TOV} = 2.18M_\odot \) and \( 2.20M_\odot \), respectively.

In previous works, within the scenario where the rotational energy of the magnetar is lost mainly via MD radiation, five NS EoSs are compared to observations to constrain the EoS (Lasky et al. 2014; Lü et al. 2015). In this work in order to compare with the constraints from GW dominated model, we follow the method of Lasky et al. (2014) and Lü et al. (2015) and 12 EoSs are compared within the MD radiation dominated model. Figure 4 presents the collapse time \( t_{\text{col}} \) as a function of proto-magnetar mass \( (M_p) \) for GRB 101219A and GRB 160821B, respectively. We find that the GM1, DD2, and DDME2 models are consistent with the current data.

Comparing the EoS constraints in the MD radiation dominated model with that of the GW dominated model, we find that the constraints are consistent with each other if the GWs are produced by the mass quadrupole deformation (Lasky et al. 2014; Lü et al. 2015). However, for the \( r \)-mode fluid oscillation model, the constraints are obviously different from that of the MD radiation dominated model. These results suggest that the NS EoS can be constrained via GW radiation loss of the rotational energy of the newly born magnetar, but the constraints are dependent on the modes of GW radiation (i.e., rigid body rotation or fluid oscillation).

### 4. Conclusions and Discussion

The observed X-ray emission internal plateau in some short GRBs suggests that a supramassive NS may survive as a remnant of double NS mergers. The supramassive NS then

![Figure 3](link)

**Figure 3.** Similar to Figure 2, but with the \( r \)-mode fluid oscillation model with \( \alpha = 0.1 \).

![Figure 4](link)

**Figure 4.** Collapse time as a function of the proto-magnetar mass for the MD dominated scenario.
collapses into a BH after a spin-down via loss of its rotation energy. In this paper, we assume that the rotational energy of the magnetar is lost mainly via GW radiation, and consider two different GW modes (i.e., mass quadrupole deformation and r-mode fluid oscillation) to constrain the NS EoS via short GRBs 101219A and 160821B. The following interesting results are obtained.

1. We derive the collapse time $t_{\text{col}}$ as a function of protomagnetar mass $M_p$ by considering the GW radiation dominated energy loss of the NS in the mass quadrupole deformation and r-mode fluid oscillation modes.

2. The NS EoS can be constrained when the energy loss of the NS is dominated by GW radiation, but with the requirement of large $\varepsilon$ (mass quadrupole deformation) and $\alpha$ (r-mode fluid oscillation) values.

3. Within the scenario where the GWs are produced by the mass quadrupole deformation, the constraints on the EoS for the GW radiation dominated model are consistent with that of the MD radiation dominated model. The data for short GRBs 101219A and 160821B point toward the GM1, DD2, and DDME2 EoSs by assuming $\varepsilon = 0.01$. However, for the r-mode fluid oscillation model with $\alpha = 0.1$, the data are different from that of the MD radiation dominated model and the correct EoS is closer to the Shen and APR models.

The assumed values of $\varepsilon = 0.01$ and $\alpha = 0.1$ are relatively large in magnitude. It seems difficult to form a magnetar with these values after a double NS merger. A maximum value of $\varepsilon = 0.001$, as well as a wide range of $\alpha \sim 10^{-5} - 0.1$, is constrained for NSs or other exotic stars (Pitkin 2011; Aasi et al. 2015). Note that the NSs examined in those papers are much older than the newly born magnetars considered in this work. On the other hand, Lasky & Glampedakis (2016) invoke observational data from short GRBs to constrain the ellipticity, and an upper limit of $\varepsilon$ can be reached at 0.01. Moreover, there is great uncertainty in our understanding of the physics of r-mode and mass quadrupole deformation of NSs (Ho et al. 2011; Lasky & Glampedakis 2016) and this increases the difficulty of probing the true values of $\varepsilon$ and $\alpha$.

From the theoretical point of view, a better way of constraining $\varepsilon$ and $\alpha$ is through detection of a GW signal and its electromagnetic counterpart in a newly born magnetar (Owen 2010; Alford & Schwenzer 2014). However, even with a large ellipticity and amplitude the GW signal produced by a newborn rapidly rotating magnetar would be difficult to detect for the current Advanced LIGO and VIRGO detectors unless the source is nearby; otherwise it may be detected by a more sensitive instrument in the future, i.e., Einstein Telescope (Alford & Schwenzer 2014, 2015; Lü et al. 2017).

Moreover, the main hypothesis of this work is that the energy released by the magnetar during the plateau phase is caused by GW radiation. Until now, there is no direct evidence to show that magnetar collapse is caused by GW radiation. However, several lines of indirect evidence suggest that GW radiation is one possible energy release mechanism for magnetar collapse. One is that the inferred initial rotation period is much longer than that expected in the double NS merger model if the energy release leading to the magnetar collapse is caused by MD radiation (Rowlinson et al. 2013 Lü et al. 2015). The other is that it is possible for a newborn magnetar from a double NS merger to have a larger ellipticity. If this is the case, a surface magnetic field of the magnetar is required to be as large as $10^{15}$–$10^{16}$ G (Rowlinson et al. 2013 Lü et al. 2015), and the higher magnetic field can result in a larger NS ellipticity (Gao et al. 2017). Lü et al. (2018) have shown that a possible signature of GW and MD radiation after the plateau was found in the X-ray light curve of GRB 060807. In order to test the hypothesis from this work, we hope that GW radiation associated with a magnetar collapse can be detected by Advanced LIGO and VIRGO in the future. Then, we can confirm whether or not the magnetar collapse after the double NS merger is caused by GW radiation.

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