Study in Development of Cans Waste Classification System Based on Statistical Approaches

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Abstract. A classification system is an initial stage in recycling cans technology. This study aims to build a cans waste classification system based on statistical approach using Red, Green, and Blue image. The image data size is reduced using principal component analysis, while the classification method used is K-Nearest Neighbors and multinomial regression. The results showed that the K-Nearest Neighbors method has the success rates of cans waste classification higher than Multinomial Regression.

Keyword: Cans, Classification, Statistical

1. Introduction
Recycling is a waste management technology that can reduce the occurrence of the pollution. The initial stage in recycling cans technology is sorting cans that will be recycled by type. In the process of sorting cans is automatically required a classification system. This paper aims to build a classification system of cans waste using Red, Green, and Blue (RGB) image based on statistical approaches.

The use of RGB image for classification has done many researchers with various methods. Widhiasih et al (2013) classifies star fruit based on RGB image using K-Nearest Neighbour (KNN) method in which the image is captured on the side position. The accuracy level is 80% if based on RG variables and accuracy of 91% if based on RGB variable. In another study, Nursalim et al (2014) classified graduate work using the K-NN method and compared its degree of accuracy with other methods of Naive Bayes (NB), Decision Tree (DT), Neural Network (NN) and Support Vector Machine SVM). The results showed that K-NN method has an accuracy of 83.33%. Specifically, the system is built on the variation of the angle of lighting, the type of lighting (lamp), and the speed of the conveyor belt. Principal Component Analysis (PCA) is used to reduce correlated variables in the data, while K-Nearest Neighbors (K-NN) and multinomial regression are used to classify cans by type.

2. Methodology
2.1. Principal Component Analysis (PCA)
Let $X$ as the vector of $p$-variables of cans waste image poses having the covariance matrix, $S$, $A$ is the eigen vector of $X$, the linear combination of $X$ and $A$,

$$Y_j = A_j^T X$$
is the $j$-th principal component if only if $\text{var}(Y_j) = A_j^T S A_j$ is maximum, with constraints $A_j^T A_j = 1$. Number of principal components in the PCA can be obtained using three ways, (1) the cumulative value of the total variance proportion, (2) correlation matrix, and (3) a scree plot.

2.2. $K$-Nearest Neighbors (KNN)

The $k$-Nearest Neighbor (KNN) method is a classification method based on the majority of the $k$-nearest neighbor categories. In the process of classifying the data is divided into training data and test data. The distance of each test data to each training data is calculated and retrieved as far as $k$ data which has the closest distance then taken the majority of the group of $k$ data which will be the group of calculated test data. In this paper, the calculation of the distance between the train data and the test data using the Euclidean Distance and Mahalanobis Distance Definition.

Suppose $x_{il}$ is the train data for the $i$-th object, $x_{ui}$ is the test data for the $i$-th object, $n$ is the number of variables the image data has, $S$ is the covariance matrix, the Euclidean Distance ($d_{ij}^E$) and the Mahalanobis Distance ($d_{ij}^M$) consecutively defined as,

$$d_{ij}^E = \sqrt{\sum_{i=1}^{n} (x_{1i} - x_{2i})^2} \quad (1)$$

$$d_{ij}^M = |(x_{1i} - x_{2i})^T S^{-1}(x_{1i} - x_{2i})| \quad (2)$$

2.3. Multinomial Regression (MR)

Let $N_{ij}$ be the random variable for $i$-th can waste with probability into $j$-th type, $\pi_j(v_i)$. The multinomial regression model was formed with stated $p(N_{i1} = |v_i) = \pi_1(v_i)$, $p(N_{i2} = |v_i) = \pi_2(v_i)$ and $p(N_{i3} = |v_i) = \pi_3(v_i)$ as the following logistic functions, where cans waste type 3 as reference category (Resti et al, 2017),

$$\pi_1(v_i) = \frac{g_1}{1 + g_1 + g_2} \quad (3)$$

$$\pi_2(v_i) = \frac{g_2}{1 + g_1 + g_2} \quad (4)$$

and

$$\pi_3(v_i) = \frac{1}{1 + g_1 + g_2} \quad (5)$$

The $g_j$ is defined as

$$g_j = \sum_{k=0}^{p} \exp(\beta_k x_{ijk}) \quad (6)$$

The regression parameters, $\beta_k$, can be estimated from the probability mass function using maximum likelihood estimation.

3. Result and Discussion

RGB image data of cans waste is obtained by capturing the can image placed on a conveyor belt on three poses; top, bottom, and side by using the camera connected to the computer with the help of MATLAB software. Let $i$ be the angle of lighting, $i=1,2,3,4$; $j$ be the lamp, $j = 1,2$, and $k$ be the speed of conveyor belt. Analysis of Variance (Anova) of the red colour pixel for the $i$-th angle, the $j$-th lamp, and the $k$-th speed is presented in Table 1.

From Table 1, it is known that there is an interaction effect between the $i$-th angle and $j$-th lamp, where with the Least Significant Difference (LSD) test it is found that the most significant treatment to the red pixel value is the 2-nd angle and the 1-st lamp, where the pixel value at the 2-nd speed has a smaller variance.
Table 1. Anova of Red Colour Pixel

| Source of variance          | df | Sum of squares | Total squares | F-stat | F table 5% |
|----------------------------|----|----------------|---------------|--------|------------|
| treatment                  | 7  | 228,2460       | 32,61         | 5,7284 |            |
| angle of lighting           | 3  | 108,6121       | 36,20         | 6,3604 | 4,35       |
| lamp                       | 1  | 43,6283        | 43,63         | 7,6647 | 5,59       |
| angle of lighting*lamp      | 3  | 76,0056        | 25,34         | 4,4509 | 4,35       |
| Kelompok                   | 1  | 4,6670         | 4,67          | 0,8199 |            |
| Galat                      | 7  | 39,8448        | 5,69          |        |            |
| Total (terkoreksi)         | 15 | 268,0909       | 17,87         |        |            |

Table 2. Anova of Green Colour Pixel

| Source of variance          | df | Sum of squares | Total squares | F-stat | F table 5% |
|----------------------------|----|----------------|---------------|--------|------------|
| treatment                  | 7  | 196,788        | 28,11         | 4,9656 |            |
| angle of lighting           | 3  | 114,3703       | 38,12         | 6,7338 | 4,35       |
| lamp                       | 1  | 14,9135        | 14,91         | 2,6342 | 5,59       |
| angle of lighting*lamp      | 3  | 67,5043        | 22,50         | 3,9745 | 4,35       |
| Kelompok                   | 1  | 7,9617         | 7,96          | 1,4063 |            |
| Galat                      | 7  | 39,6306        | 5,66          |        |            |
| Total (terkoreksi)         | 15 | 236,4186       | 15,76         |        |            |

Table 3. Anova of Blue Colour Pixel

| Source of variance          | df | Sum of squares | Total squares | F-stat | F table 5% |
|----------------------------|----|----------------|---------------|--------|------------|
| treatment                  | 7  | 154,0464       | 22,01         | 5,7556 |            |
| angle of lighting           | 3  | 95,0234        | 31,67         | 8,2841 | 4,35       |
| lamp                       | 1  | 3,8027         | 3,80          | 0,9945 | 5,59       |
| angle of lighting*lamp      | 3  | 55,2203        | 18,41         | 4,8141 | 4,35       |
| Kelompok                   | 1  | 5,5920         | 5,59          | 1,4625 |            |
| Galat                      | 7  | 26,7648        | 3,82          |        |            |
| Total (terkoreksi)         | 15 | 180,8112       | 12,05         |        |            |

Table 2 shows that only the angle affects the color of green RGB image pixels. Based on the LSD test it is known that the 4th angle most significantly affects the green pixel value, where the pixel value at the 2-nd speed and the 1-st lamp has the smallest variance.

From Table 3, it is found that there is an interaction effect between the i-th angle and the j-lamp. Based on LSD test it is known that the most significant treatment to the blue pixel value is the 2-nd angle and the 1-st lamp. Then, the data of the cans image at the both 2-nd and 4-th angles for each of the 1-st lamps and the 2-nd speed are taken as further analysis data. Each of these data is then divided into training data and test data.

Suppose that the independent variable of the RGB cans waste image pixel poses consists of a red top (C₁), a red bottom (C₂), a red side (C₃), a green top (C₄), a green bottom (C₅), a green side (C₆), a blue top (C₇), a blue bottom (C₈), and a blue side (C₉). Considering the scree plot shown in Fig. 1 and the total variance proportion shown in Table 4, it was decided that the number of PCs is 2. The first PC usage was able to explain the variance of the 86.8% data. By using Minitab software obtained eigenvalues of independent variables are $\lambda₁ = 771,67$, $\lambda₂ = 84,83$, $\lambda₃ = 11,25$, $\lambda₄ = 6,99$, $\lambda₅ = 6,67$, $\lambda₆ = 3,48$, $\lambda₇ = 2,98$, $\lambda₈ = 0,90$ and $\lambda₉ = 0,49$. These values show that all pixel colors have the contribution is almost the same but the red color pixels have the biggest contribution. The use of a second PC capable of explaining the variance of 96.3% data also indicates that red pixels have the...
greatest contribution, however, when viewed from their eigenvalues the values are against the green and blue pixel values.

![Scree plot between component number, $p$, and eigenvalue, $\lambda_p$.](image)

**Figure 1.** Scree plot between component number, $p$, and eigenvalue, $\lambda_p$.

**Table 4.** Total variance proportion

| Total variance proportion | 86.8% |
|---------------------------|-------|
| Total variance proportion | 96.3% |
| Total variance proportion | 97.6% |

Table 5 present the classification result using both KNN and MR method. Each of data is divided into training data (50%) and test data (50%). For data without treatment and data with treatment of 4-th angle, 1-st lamp, 2-rd speed, the KNN method has a higher success rate than MR method, but for data with treatment of 2-th angle, 1-st lamp, 2-rd speed, the KNN method has a lower success rate than MR method.

**Table 5.** The success rate of cans waste classification using KNN and MR method

| No. | Data                          | Classification method | Success Rate of Classification |
|-----|-------------------------------|-----------------------|--------------------------------|
| 1   | without treatment             | KNN                   | 70.4%                          |
|     |                               | MR                    | 56.0%                          |
| 2   | 2-th angle, 1-st lamp, 2-rd speed | KNN                | 59.2%                          |
|     |                               | MR                    | 64.8%                          |
| 3   | 4-th angle, 1-st lamp, 2-rd speed | KNN                | 51.2%                          |
|     |                               | MR                    | 49.6%                          |

4. Conclusion

This study builds a cans waste classification system based on statistical approach using Red, Green, and Blue image. Considering the scree plot and the total variance proportion, we have 2 principal components (PC). The first PC was able to explain the variance of the 86.8% data, where all pixel colors have the contribution is almost the same but the red color pixels have the biggest contribution. The second PC was able to explain the variance of the 96.3% data where all pixel colors have also the contribution is almost the same but, the values are against the green and blue pixel values. For cans waste classification system, generally, the KNN method has a higher success rate than MR method.
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