FANPCE TECHNIQUE FOR RISK ASSESSMENT ON SUBWAY STATION CONSTRUCTION

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Abstract. Risk assessment is critical for the construction of the subway station to improve the risk management and reduce the additional loss. According to field investigation of safe construction, the analytical network process (ANP), fuzzy set theory and fuzzy comprehensive evaluation (FCE), a fuzzy ANP comprehensive evaluation (FANPCE) model was proposed to evaluate the risk of subway station construction in this paper. Twelve key risk factors of subway station construction were identified through literature review and questionnaires. The interdependency among risk factors were illustrated through the network structure of ANP, and then a weight matrix of single risk factors was built by comments and survey results, and the interdependent weight matrix was quantified by integrating the triangular fuzzy number into the ANP. Subsequently, the total risk rank of assessed projects can be quantified though the synthesis of weight matrices with the synthetic operator of FCE. Wu Lu Kou subway station was selected as a case study. The results imply that, construction experience, underground water, and safety consciousness have a substantial influence on construction projects and that the total construction risk of Wu Lu Kou subway station is ranked at I level. Moreover, the loss analysis of the whole construction process verifies this method. In addition, the developed fuzzy set theory-ANP-FCE integrated network provides stakeholders a consolidated model for the risk evaluation.

Keywords: construction risk, subway station, risk identification, ANP, risk assessment, FANPCE method.

Introduction

Subterranean engineering, especially the subway engineering, is an effective method to alleviate the traffic congestion. Statistically, approximately 2476 subway stations and 4136 subway km have been constructed or are planned from 2014 to 2021 in 23 cities of China (Hu & Qin, 2013; H. R. Li, Q. M. Li, & Lu, 2017). However, the complicated construction environment, immature construction techniques and inadequate construction experience can probably result in project delay, additional cost and engineering accidents (Qian, 2012; Xiong, Lu, Wang, Qian, & Rong, 2018). Figure 1 shows the data of subway accidents in China from 2003 to 2017 according to the official data and literature (Li, Du, & Zhang, 2014; Li et al., 2017). Since 2011, the number of subway accidents and casualties has increased as shown in Figure 1.

Therefore, it is critical to improve the risk management techniques in the construction of subway stations, so as to reduce the risk and ensure the construction safety. The risk assessment of subway construction has been investigated by many scholars, and many methods have been employed to assess the probability of construction risk. Mahamid (2011) ranked risk events by Risk Matrix (RM) based on qualitative analyses of risk components. However, the risk classification is limited to a number of categories in this method. According to FTA, Zhang, Wang, and Hu (2011) assessed the safety of row piles in excavation engineering; while FTA must identify the accurate failure rate of each event (Li et al., 2018), and FTAs established by different people have different results. Roy (2010), Nyvlt, Prívara, and Ferkl (2011) presented scenario analysis methods that
can test possible consequences for alternative scenarios in a project, but a lot of data were required to evaluate the probability of an event. The work breakdown structure (WBS)-based method (Klein, Powell, & Chapman, 1994; Seyedhoseini, Noori, & Hatefi, 2009) analyzes construction risk by dividing the total risk into many smaller risks (Ma, Rezania, Yu, & Bai, 2017; Ma, Cai, Zhou, & Li, 2018a). Moreover, it is difficult to determine the WBS for some complicated projects and quantize the risk by the single WBS-based method. Kuo and Lu (2013) employed a FMCDM approach (the integration of consistent fuzzy preference relations and fuzzy multiple attributes direct rating) to systematically assess risk for the metropolitan construction.

Considering the limitations of existing methods, further research on the risk assessment should be performed from other perspectives. AHP, fuzzy AHP, and AHP-ANP are prevailing methods for decision-making analysis (Jie, Hu, Q. Y. Li, & G. X. Li, 2004; Zhao, Chen, Pan, & Lu, 2017). The elements of a system can be aggregated into hierarchical or element groups that have similar properties without interactions or dominance relationships among elements within a hierarchy (Saaty, 2001; Guo, Shang, & Li, 2011). Sharma, Roy, Kar, and Prentkovskis (2018) evaluated the performance of Indian railway stations (IRS) through integrating rough numbers, AHP and multi-attribute border approximation area comparison (MABAC) methods in rough environment. Roy, Chatterjee, Bandyopadhyay, and Kar (2018) proposed a systematic evaluation and assessment approach by incorporating ANP and multi-attributive border approximation area comparison methods in the rough environment. In the practical application, however, the elements of a system are generally connect-

Figure 1. Statistics of subway accident in China from 2003–2017

ed rather than organized in a hierarchical structure, then a network structure with a preferable form is produced. The ANP technique enables more complex relationships among decision levels, attribute, analyses of the uncertainty and ambiguity of a system and project (Saaty, 2001; Chu et al., 2017; Tavana, Zandi, & Katehakis, 2013; Chatterjee, Bandyopadhyay, Ghosh, & Kar, 2015; Bu-Qammaz, Dikmen, & Birgonul, 2009). Since risk factors are indeterminate, abstract, and uncertain, it is difficult to quantify risk factors. Considering the impact of all risk factors comprehensively, Fuzzy comprehensive evaluation (FCE) can assess the total risk, distinguish the importance of various factors by the weight setting and the possible risk determination with various degrees. The maximum influence is the final determination value of the risk level (Chu et al., 2017). Li et al. (2014) and Ying, Wang, Zhu, Lei, and Qin (2016) ranked subway construction risks by a FCE model. However, compared with ANP, the interdependent and mutually restrictive relationships among risks are not fully considered. In summary, the following conditions have not been fully considered in the previous research:

- The total risk of the project is the superposition and compounding of each sub-risk, as any risk generation will have a varying impact on the overall objectives of the project. Therefore, it is necessary to identify risk factors for different projects by certain methods.
- There is an interdependent and mutually restrictive relationship between risks that need to be fully considered.
- Risk and risk analysis of subway station projects is usually dynamic throughout the entire process of project construction.
Accident analyses and field investigations of safe construction can effectively identify the risk factors for subway station projects. ANP technique handles interactions among elements by obtaining the composite weights via the development of a super matrix (Dağdeviren, Yüksel, & Kurt, 2008; Chatterjee, Zavadskas, Tamošaitienė, Adhikary, & Kar, 2018). Triangular fuzzy numbers (TFNs) derived from the concept of Dev fuzzy sets can effectively quantify the uncertainty and ambiguity. The fuzzy comprehensive evaluation (FCE) can transform the fuzzy relations between evaluated risk factors and evaluated projects into a fuzzy relationship between the evaluated project and the evaluation grade.

Thus, the main objectives of this research are as follows:
- Identifying and classifying risk factors of subway construction projects based on statistics and site risk investigation with effective questionnaires.
- Developing a logical model integrating fuzzy set theory, ANP, and FCE for risk assessment for the subway station construction.
- Assessing the risk level of subway station construction based on the FANPCE method in different construction processes.

This paper is organized as follows. The FANPCE method is introduced in Section 2. Details of the development of the FANPCE model are provided in Section 3. The application of the model and the construction risk evaluation of Wu Lu Kou subway station are presented in Section 4. Section 5 discusses these findings, and Section 6 presents the conclusions.

1. Literature review

MCDM methods and improved method have been extensively applied in the realm of project risk management, and optimized to process various types of uncertainties encountered in the decision-making process. Antuchevičienė, Zavadskas, and Zakarevičius (2010) supplemented TOPSIS (Technique for the Order Preference by Similarity to Ideal Solution) method and integrated the Mahalanobis distance in the usual algorithm of TOPSIS for investigating multiple criteria construction management decisions issue. Vafadarkinjoo, Mobin, and Firouzabadi (2016) presented an intuitive fuzzy decision-making trial and evaluation laboratory (DEMATEL) to prioritize risks associated with construction projects by the risk breakdown structure. Debnath, Roy, Kar, Zavadskas, and Antucheviciene (2017) combined modified grey DEMATEL, Multi-Attribute Border Approximation area Comparison and sensitivity analysis to evaluate and select the genetically modified agro portfolio. Zavadskas, Turskis, and Tamošaitiene (2010) presented risk assessment of construction projects by applying TOPSIS gray and COPRAS-G methods based on multi attribute decision-making methods. Taylan, Bafail, Abdulaal, and Kabli (2014) developed hybrid methodologies based on fuzzy AHP and fuzzy TOPSIS and applied the relative importance index method to prioritize the project risks based on the obtained data. Yang, Said, Lin, and Zheng (2018) presented a novel methodology to determine the overall highway safety level through statistical analysis and ANP with set pair analysis (SPA). D. Shin, Y. Shin, and Kim (2016) performed a comparative analysis of AHP and fuzzy AHP to evaluate the potential risk factors at the construction site of a nuclear power plant. Santos and Jungles (2016) evaluated the completion of construction project risk by considering the correlation of delay and the schedule performance index along with any time overrun. Ahmadi, Behzadian, Ardeshir, and Kapelan (2016) analyzed the criteria to prioritize potential risk events and quantified them by fuzzy AHP. Ulubeyli and Kazaz (2016) developed a fuzzy-based subcontractor selection model for globally based construction projects. Lin, Chen, and Chuang (2016) presented a Hybrid Multiple Criteria Decision-Making Model by combining DEMATEL with D-ANP (DEMATEL based ANP) and VIKOR methods to improve project risk management. Chatterjee et al. (2018) extended the ANP methodology in the D numbers domain to handle three types of ambiguous information. Valipour, Yahaya, Noor, Antucheviciene, and Tamošaitiene (2017) proposed a Stepwise Weight Assessment Ratio Analysis based on a Complex Proportional Assessment framework to assess Iranian construction project risk. Chatterjee and Kar (2018) evaluated and ranked the potential alternatives by Grey-Based Complex Proportional Assessment Method.

In contrast to the abovementioned studies, this paper develops a FANPCE method by integrating ANP, triangular fuzzy numbers and FCE to assess the risk level of a subway station project.

2. Research method

2.1. Analytical Network Process

AHP technique is commonly employed for evaluating the weights of risk (Shin et al., 2016). This method employs pairwise comparisons among criteria based on expert opinions and determines the relative weights of the criteria (Saaty, 1999; Zhao et al., 2017). However, as noted by Meade and Sarkis (2002) the relationship among decision levels and attributes is ignored by AHP. Subsequently, ANP was improved by Saaty (1999) in line with AHP. Decision theories of ANP and AHP are essentially identical; the only difference between ANP and AHP is that, the former establishes a network model, whereas the latter establishes a hierarchical model (Bayazit, 2006). ANP applies and analyzes a super matrix for weight synthesis (Saaty, 2004; Zhao et al., 2017). The representation of the network model and the weight synthesis are the two main components of ANP method (Saaty, 2004; Yang et al., 2018). The structure of ANP model can be represented in the graphical form (which qualitatively represents the interactional relationships and feedback among the components) and matrix form (which qualitatively represents the degree or magnitude of the interaction or feedback).
2.2. Fuzzy set theory

In most cases, the complexity of decision problems prevents the understanding of these problems with certainty (Bjegović, Krstić, & Mikulić, 2006; Son, 2018). Fuzzy set theory, introduced by Zadeh (1965), enables the simultaneous treatment of imprecise and precise variables. Triangular fuzzy numbers, which are derived from the concept of Dev fuzzy sets (Zadeh, 1965), are applied to manage the quality and risk to solve the problems of an uncertain environment (Zimmerman, 2001). A fuzzy number is the fuzzy set \( F = \{ x \in R | \mu_F(x) \} \), where \( x \) is in the real line. The value form \( R : -\infty < x < +\infty \) and \( \mu_F(x) \) is assumed as a continuous function map. A triangular fuzzy number (TFN) can be defined by the triplet \((l, m, u)\) and the membership function (1); the membership function \( \mu(x) \) can obtain values in the range \([0,1]\) (Zimmerman, 2001; Lan & Zhang, 2006).

\[
\mu_F(x) = \begin{cases} 
0, & x < l \cdot \text{or} \cdot x > u \\
(x-l)/(m-l), & l \leq x \leq m \\
(x-u)/(m-u), & m \leq x \leq u 
\end{cases}
\]

where \( l \) and \( u \) respectively denote the lower bound and upper bound of the ambiguity degree of the judgment of \( m \), and \( m \) represents the mid-value \((l \leq m \leq u)\).

2.3. Fuzzy comprehensive evaluation

FCE method is one type of application of fuzzy mathematics (Zadeh, 1965). The basic concept of the risk evaluation of a project is described as follows: (1) consider the impact degree of all risk factors comprehensively; (2) distinguish the importance of various factors by setting weights; and (3) determine various degrees of risk possibility, in which the maximum degree is the final determination value of the risk level (Chu et al., 2017). The accuracy and reliability of the comprehensive evaluation result depend on the reasonable selection of factors and weight distributions (the weights will vary with different states and timing of the factors), synthesis of a comprehensive evaluation, and representation of results and the selection process (Dai & Li, 2016).

2.4. FANPCE

Firstly, in this study, the identification of risk factors is conducted through accident analyses and questionnaires, which are designed to refine risk factors. Secondly, the occurrence of a risk event is attributed to the interaction of many factors. These factors can be coordinated with the characteristics of the structural model of ANP method, revealing the relationships among levels. Thirdly, ANP technique is adopted to establish the network structure model of risk factors. The relationships among the levels in the ANP model are assessed by the on-site engineers; Furthermore, the TFN method is used to address the vague and unquantifiable opinions of respondents. Finally, the weight of risk factors is calculated, and the fuzzy synthesis operator is used to evaluate the construction risk comprehensively. FANPCE, derived from the integration of ANP, fuzzy set theory and FCE, is a quantification method for estimating the uncertainty and ambiguity. Figure 2 shows the risk evaluation with the combination of ANP, field investigation of safe construction, fuzzy set theory and FCE. The detailed process of FANPCE is discussed in the following section.

3. Method development

3.1. Establishment of comment set for subway station construction risk

Since the final evaluation result is the evaluation vector, the construction risk of a subway station can be rated based on the maximum membership principle (Dai & Li, 2016). Therefore, the construction risk evaluation vector \( V = \{v_1, v_2, ..., v_n\} \) and comment set construction risk \( P = \{I, II, III, IV\} \) are assumed to represent the information on the membership degree of each comment level corresponding to the evaluated project. The degree of membership information corresponding to each comment level of the evaluated object is represented by this vector. If \( v_i = \max \{v_s\} \), then the rating of construction risk of the subway station is \( I \). The method separates the comments into four levels to build a comment set for subway station construction risk, i.e., \( P = \{I, II, III, IV\} \). Table 2 shows the criteria of risk rank.

3.2. Establishment of comment set for subway station construction risk

The establishment of the network structure of the FANPCE method is based on the following process.

Step 1. Categorize the percentage of subway construction hazards.

Based on 178 subway construction accidents in China from 2003–2017 (Hu & Qin, 2013; Li et al., 2014; Li et al., 2017), as shown in Figure 1, the categories and percentages of subway construction accidents are obtained in Figure 3(a). Accidents are classified as the collapse, falling, vehicle injury, lifting injury, object strike, electric shock and mechanical injury. Besides, the collapse is the most frequent accident in subway construction.

Step 2. Analyze the causes of accidents and categorize risk factors.

The causes of 178 accidents are divided into five categories: personnel risk, material risk, mechanical risk, environmental risk and system risk. The relevant percentages are shown in Figure 3(b). Then, risk factors of subway station construction are summarized based on the data of 178 subway accidents. Five first-level risk factors, ten second-level risk factors and 25 TLRF are identified, as shown in Figure 4.

Step 3. Design the questionnaire and field risk investigation.

If these factors are incorporated into an ANP network structure, the quantification of risk by the ANP network
structure is difficult, and the risk factor classification needs to be further verified. Therefore, a field risk investigation should be conducted to refine the ANP network structure, simply the calculation and verify the correctness of the statistical data.

Consequently, a questionnaire is designed for the risk identification during the subway station construction, as shown in Table 1. Design principles include that, the identification of accident types, location of occurrence, causes of accidents, loss ranks, risk probability and risk tolerability framework. Nine stations that are under construction along the subway line 4 in Xi’an, Shan’xi Province, China, are selected to conduct the field investigation of safe construction. Figure 5 shows the location of the field investigation. 40 engineers of relevant disciplines and 10 professors of engineering management at university were investigated.

Based on the Guidelines for Tunneling Risk Management, creating risk rank and risk acceptance criteria (Eskesen, Tengborg, Kampmann, & Veicherts, 2004; Feng, Li, & Rostami, 2019) for subway station construction hazards (Ma, Cai, Li, & Duan, 2018b; Ma, Duan, Liu, Li, & Zhou, 2019) involves the simple classification of subway station accidents, as shown in Table 2. Note that weightings or combinations of different risk factors are not involved in this classification.

Subsequently, the field investigation of construction risk is carried out by analyzing potential risk events and
L. Wu et al. FANPCE technique for risk assessment on subway station construction

Table 1. Questionnaire about risk identification for subway station construction

| Serial number | Risk register | Location of occurrence | Risk factors | Loss ranks | Risk probability | Risk tolerability framework | Notes |
|---------------|---------------|-------------------------|--------------|------------|-----------------|----------------------------|-------|
| 1 (example)   | falling       | construction scaffold   | First-layer factor \( (B) \); Second-layer factor \( (B_1) \); Third-layer factor \( (B_{11}) \) | C          | 3               | III                        |       |
| 2             |               |                         | First-layer factor (); Second-layer factor (); Third-layer factor () |            |                 |                            |       |

Note: Form filling explanation: Listing the risk factors based on Figure 4, the value of loss rank, risk tolerability framework and risk probability are based on Table 2. If Figure 4 and Table 2 do not list your choice, please indicate an explanation in the notes.

Figure 3. Risk factors analysis: (a) categories and percentages of subway construction accidents; (b) causes and associated percentages of subway construction accidents

Table 2. Risk rank and risk acceptance criteria

| Frequency rank | Risk acceptance criteria | Disposal principle                                                                 | Control plan                                                                                       | Response department |
|----------------|--------------------------|------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------|---------------------|
| Disastrous     |                          | Risk control measures must be implemented to reduce risk. The risk should be reduced to acceptable levels or negligible levels. | The risk warning and the emergency response plan should be prepared or revised and adjusted.       | Government authorities and Construction parties                                                    |
| A              | Unacceptable             | Risk control measures must be implemented to reduce risk. The risk should be reduced to acceptable levels or negligible levels. | The risk warning and the emergency response plan should be prepared or revised and adjusted.       | Government authorities and Construction parties                                                    |
| B              | Unwanted                 | Risk management should be implemented to reduce risk, and the cost of risk reduction should not exceed the loss caused by the risk. | Risk prevention and monitoring and risk management measures should be implemented.                 | Construction parties                                                                 |
| C              | Acceptability            | Implementing risk management and taking management measures.                        | Strengthen daily management and monitoring.                                                        | Construction parties                                                                 |
| D              | Negligible               | Implementing risk management.                                                       | Performing daily inspection.                                                                       | Construction parties                                                                 |
| E              |                          |                                                                                    |                                                                                                    |                      |
Figure 4. The hierarchical structure of risk factors
Figure 5. Location of field investigation

Figure 6. Field investigation of risk events
occurred risk events in the subway construction. Figure 6 reveals the following partial risk events caused by (1) hazy weather, which can delay the project; (2) the narrow site, which can slow the construction and increase the safety risk and material turnover cost; (3) the rain and lack of drainage capacity, then the loess is changed as flowing soil, which can increase measurement costs and result in delays; (4) pipelines of different types with different orientations and depths, which can increase the measurement cost and result in delays; (5) the government to control the environmental pollution; (6) workers without safety precautions; (7) dangerous operations, such as steel stull butt joint welding and gantry crane operation transported heavy machinery; (8) heavy traffic and numerous tall buildings that surround the site limited construction. These findings help identify risk factors and understand the risk events in subway station construction.

Step 4. Build a network structure of risk factors for subway station construction.

Engineers and professors in relevant disciplines were selected to complete a questionnaire of field investigation in line with Figure 4 and Table 2. Forty valid questionnaires were collected. Based on the results, the weights of the 25 third-level risk factors were calculated. Figure 7 shows calculation results. Based on the weights (ranks I–IV) of the 25 TLRF from the field investigation, risk weights of rank I for most risk factors in the field investigation are slightly smaller than previous estimates, and weight distributions are generally consistent; risk weights of rank II are slightly larger than previous estimates, and weight distributions are generally consistent; risk weight distributions of rank III are generally consistent; and weight distributions of rank IV are slightly different. Therefore, the 25 TLRF are generally suitable as risk factors for subway station projects. Based on the results and safety assessments, risk factors with greater weights, i.e., ranks I and II, are selected to simply the risk factor analysis. Then, the network structure of the FANPCE model is established based on the simpli-
Figure 8. ANP network structure of the risk factors of subway station construction

3.3. Weights

Step 1. Build a fuzzy relational matrix for a single factor.

Twelve TLRF are evaluated by building a fuzzy relational matrix, which consists of the fuzzy relation from V to P corresponding to the probability of generating risk, the loss degree caused by the risk and controllability of the risk based on Table 2. Then, the investigated data are weighted to obtain the fuzzy relational matrix of a single factor \( R_i \) (Eqn (2)):

\[
R_i = \begin{bmatrix}
R_{0iV1} & R_{0iV2} & \cdots & R_{0iVj} \\
R_{1iV1} & R_{1iV2} & \cdots & R_{1iVj} \\
\vdots & \vdots & \ddots & \vdots \\
R_{6iV1} & R_{6iV2} & \cdots & R_{6iVj}
\end{bmatrix}
\]

where \( j \) is the number of TLRF. Taking the probability of generating risk, the loss degree and the controllability of the risk as criteria, \( R_{0jV1} \) consists of weights of each TLRF at risk level I; \( R_{0jV2} \) consists of weights of each TLRF at level II; \( R_{0jV3} \) consists of weights of each TLRF at risk level III; \( R_{0jV4} \) consists of weights of each TLRF at risk level IV. Taking the probability of generating risk as an assessment criterion, \( R_p \) is the fuzzy relational matrix, and the relevant data is provided from the survey; \( R_L \) and \( R_C \) are the obtained fuzzy relational matrices based on the loss degree and controllability of the risk. \( R_p \), \( R_L \), and \( R_C \) are integrated to obtain the weight matrix \( R \), where

\[
R = 1/3(R_p + R_L + R_C)
\]

Step 2. Calculate the weight vector of risk factors.

Step 2.1. Build a FCM.

Interactional relationships among the ANP levels are assessed in line with the opinions of experts and engineers; however, the respondents' opinions are vague and unquantifiable. Here, the TFN method is used to address this issue. Dispersion membership is used to evaluate the object, the membership function of relative importance is represented in Table 4. First, the FCMs among twelve TLRFs are built. The factor \( U_{12} \) is taken as the criterion, the incidences of \( U_{11} \), \( U_{12} \) and \( U_{13} \) for \( U_{12} \) are compared for
are obtained \((7)\). (7)

Based on this analysis, the fuzzy weight vector is calculated by the characteristic root method. Forthermore, the fuzzy weight vector \(\{w_{12}^2, w_{12}^3, w_{13}^3\}^T\) is also the priority vector of the effect of \(U_{11}, U_{12}\) and \(U_{13}\) on \(U_{12}\). At the same time, the weight vector \(\{w_{11}^2, w_{13}^2, w_{13}^3\}^T\) of \(B_{11}\) and \(\{w_{12}^2, w_{12}^3, w_{13}^3\}^T\) of \(B_{12}\) are calculated. Next, the FWM \(W_{11}^E\) (Eqn (7)) of the factor set \(U_1\) can be obtained by combining \(\{w_{11}^2, w_{12}^2, w_{13}^2\}^T\), \(\{w_{11}^2, w_{11}^1, w_{11}^3\}^T\), and \(\{w_{11}^2, w_{13}^2, w_{13}^3\}^T\).

The calculation is repeated in the same way, the FWMs of \(W_{12}^E, W_{13}^E, W_{21}^E, W_{22}^E, W_{23}^E, W_{24}^E, W_{31}^E, W_{32}^E, W_{33}^E, W_{34}^E, W_{41}^E, W_{42}^E, W_{43}^E, W_{44}^E\) are obtained according to calculation of the weight vectors of FCMs (Eqn (8)).

The FWMs are combined to constitute the unweighted fuzzy super matrix \(W\) (Eqn (8)).

Step 2.3. Build the fuzzy weight matrix of elements of second-level factors.

Since the fuzzy super matrix \(W\) is not normalized, the calculation of the weight of subblock \(W_{ij}\) of \(W_{ij}\) is necessary. The pairwise blocks are compared to build the FCM, so as to obtain the normalized sort vector \(A\) per subblock \(W_{ij}\). \(a_{ij}\) represents the weight of sub-block \(i\) and \(i\) affects sub-block \(j\), and \(a_{ij} = 0\) indicates there is no effect. As the method in step 2, taking risk factors \(U_1, U_2, U_3,\) and \(U_4\) as the criteria, the relative importance of \(U_1, U_2,\) \(U_3,\) and \(U_4\) is compared to build FCMs (Eqn (9)). Then, FWM \(A\) of FCMs (Eqn (9)) is calculated.
The fuzzy weighted super matrix \( W \) (Eqn (10)) can be built based on the fuzzy super matrix \( W \) and the FWM \( A \):

\[
W = A \times W = \begin{bmatrix}
\begin{array}{cccc}
11 & 12 & 13 & 14 \\
11 & 12 & 13 & 14 \\
21 & 22 & 23 & 24 \\
31 & 32 & 33 & 34 \\
41 & 42 & 43 & 44 \\
\end{array}
\end{bmatrix}
\begin{bmatrix}
R_{11} & R_{12} & R_{13} & R_{14} \\
R_{21} & R_{22} & R_{23} & R_{24} \\
R_{31} & R_{32} & R_{33} & R_{34} \\
R_{41} & R_{42} & R_{43} & R_{44} \\
\end{bmatrix}
\begin{bmatrix}
11 & 12 & 13 & 14 \\
11 & 12 & 13 & 14 \\
21 & 22 & 23 & 24 \\
31 & 32 & 33 & 34 \\
41 & 42 & 43 & 44 \\
\end{bmatrix}
\]  

(10)

### 3.4. Calculation of the limit order sector

The limit order sector \( T \) can be obtained by multiplying it with itself until the normalisation eigenvector of the super matrix \( W \) corresponds to the eigenvalue 1 with Eqn (11) (Saaty, 2004; Dağdeviren et al., 2008; Tavana et al., 2013).

\[
T = \lim_{n \to \infty} W^n,
\]

where \( T \) is the limit order sector; \( W \) is the weighted super matrix; \( n \) is the exponent determined by iteration. The final priorities of risk factors can be shown in the corresponding columns in the limit order sector.

### 3.5. Assessment on the risk level of construction

The construction risk level of the project is assessed through the FCE model in Eqn (12):

\[
V = T \circ R,
\]

where \( V \) represents the evaluation result vector, which is the description of the comprehensive risk level of evaluation projects; \( R \) represents fuzzy relation matrix, and the evaluation result of single risk factor; \( T \) represents the evaluate weight vector of the risk factor obtained through FANPCE, describing the relative importance of risk factors toward the evaluation object; \( \circ \) represents a fuzzy synthesis operator, synthesizing \( T \) and \( R \). In addition, the multiplication and bounded operator \( M(\circ, \oplus) \) of fuzzy mathematics operation theory are adopted (Dai & Li, 2016). The formula describes that fuzzy relations \( T \) of evaluation risk factors and evaluation projects are transformed into the fuzzy relationship \( V \) between the evaluated project and the evaluation grade through fuzzy transducer \( R \), which represents the fuzzy relation of the evaluation risk factors and the evaluation risk level. The comprehensive evaluation matrix \( V \) can be determined by Eqn (12) and by acquiring the value of \( \max(v_i / \sum v_j) \) (maximum membership) (Saaty, 2004; Wang & Hak-Keung, 2018), which is the evaluation of the model.

### 4. Case study

#### 4.1. Project backgrounds

Wu Lu Kou station is a transfer station between subway line 1 and subway line 4 in Xi'an. The location of the station is shown in Figure 5. The average excavation depth of the foundation pit is 23.1 m, and the main volume of the foundation pit is 83273 m³. The construction structure of the station involves bored piles, internal supports, temporary central piles and temporary cover systems which comprise prefabricated steel girders. These components constitute a complex and narrow construction space, resulting in a high probability of risk events, as shown in Figure 6. Therefore, investigating the construction risk is necessary for subway station project to improve the efficiency. The total construction risk of this subway station was assessed by the FANPCE method on 12/2013.

#### 4.2. Results and analysis

Twenty engineers of relevant disciplines associated with the Wu Lu Kou station were selected to evaluate the sub-elements based on a comment set and Table 2. The investigated sub-element results in line with the probability of generating risk are presented in Table 3. By weighting the data in Table 3, the fuzzy relational matrix \( R_p \) is built, as described in this section. In the same way, the fuzzy relational matrices \( R_L \) and \( R_C \) can be obtained. Finally, the matrices \( R_L, R_C, \) and \( R_p \) are integrated to obtain the weight matrix \( R \). These results are presented as follows:

|  |  |  |  |  |
|---|---|---|---|---|
| 0.65 | 0.25 | 0.05 | 0.05 | 0.7 | 0.15 | 0.15 | 0 |
| 0.55 | 0.35 | 0.05 | 0.05 | 0.65 | 0.2 | 0.15 | 0.05 |
| 0.6 | 0.35 | 0.05 | 0.05 | 0.35 | 0.15 | 0.15 | 0.05 |
| 0.05 | 0.05 | 0.15 | 0.25 | 0.05 | 0.15 | 0.15 | 0.05 |
| 0.6 | 0.35 | 0.05 | 0.05 | 0.05 | 0.15 | 0.15 | 0.05 |
| 0.3 | 0.35 | 0.05 | 0.05 | 0.05 | 0.15 | 0.15 | 0.05 |
| 0.7 | 0.2 | 0.1 | 0.1 | 0.7 | 0.2 | 0.1 | 0.1 |
| 0.25 | 0.3 | 0.1 | 0.1 | 0.25 | 0.3 | 0.1 | 0.1 |

|  |  |  |  |  |
|---|---|---|---|---|
| 0.75 | 0.2 | 0.05 | 0.05 | 0.7 | 0.2 | 0.08 | 0.02 |
| 0.5 | 0.3 | 0.25 | 0.25 | 0.57 | 0.25 | 0.15 | 0.02 |
| 0.6 | 0.3 | 0.1 | 0.1 | 0.67 | 0.25 | 0.07 | 0.02 |
| 0.1 | 0.1 | 0.55 | 0.25 | 0.08 | 0.13 | 0.48 | 0.3 |
| 0.35 | 0.45 | 0.15 | 0.05 | 0.18 | 0.33 | 0.27 | 0.22 |
| 0.2 | 0.15 | 0.15 | 0.15 | 0.05 | 0.12 | 0.37 | 0.47 |
| 0.1 | 0.1 | 0.45 | 0.35 | 0.05 | 0.12 | 0.37 | 0.47 |
| 0.75 | 0.15 | 0.1 | 0.1 | 0.48 | 0.32 | 0.13 | 0.07 |
| 0.1 | 0.05 | 0.1 | 0.15 | 0.08 | 0.1 | 0.05 | 0.32 |
| 0.4 | 0.3 | 0.2 | 0.1 | 0.43 | 0.37 | 0.1 | 0.1 |
| 0.7 | 0.15 | 0.1 | 0.05 | 0.63 | 0.22 | 0.1 | 0.05 |
| 0.5 | 0.2 | 0.25 | 0.35 | 0.37 | 0.18 | 0.28 | 0.17 |

The fuzzy relational matrix \( R \) of a single factor reveals that, the risk rank 1 weights of 12 TRLF are ordered as \( U_{11} > U_{13} > U_{42} > U_{12} > U_{32} > U_{41} > U_{43} > U_{23} > U_{22} > U_{31} = U_{23} > U_{31} \), and the risk factors (construction experience, safety awareness, and underground water) are considered as high-risk factors of the single assessed factors. The risk
The limit order sector $\mathbf{T}$ is as follow:

$$
\mathbf{T} = \begin{bmatrix}
0.1266 & 0.0896 & 0.1076 & 0.0327 & 0.0332 & 0.0172, & 0.0426 & 0.1087, & 0.0388, & 0.0693, & 0.2407, & 0.0930
\end{bmatrix}^T.
$$

Which is also the final weight of 12 TLRF. The final weights of 12 TLRF are ordered as $U_{42} > U_{11} > U_{32} > U_{13} > U_{43} > U_{12} > U_{41} > U_{33} > U_{22} > U_{21} > U_{23}$, the result reveals that the weight of underground water is the biggest. Therefore, it should be a focal risk factor, whose influence can also be verified in the field risk investigation as shown in the Figure 6. The rain and lack of drainage capacity made the loess become flowing soil, which increased measurement costs, the delay of the construction and the decrease of the foundation stability. In addition, the con-
struction, organization system and safety awareness also play important roles in risk events. Meanwhile, the result also reveals that maintenance conditions is the least sensitive parameter in risk events.

Then, based on $V = [0.4991, 0.2370, 0.1642, 0.1001]^T$, results can be obtained. The weight of rank I is 0.4991, i.e., the maximum; the weight of rank II is 0.2370; the weight of rank III is 0.1642; and the weight of rank IV is 0.1001. Based on the maximum membership principle that $\max\left(\frac{v_i}{\sum_{i=1}^n v_i}\right)$ is the total risk rank of the assessed project, the construction risk rank of the Wu Lu Kou subway station is I. Thus, the risk is unacceptable based on Table 2. Government authorities and construction parties should implement additional risk control measures to reduce risk to the acceptable or negligible levels, and prepare or revise the risk warning and emergency response plan.

Furthermore, when finishing the risk assessment of this subway station in 2013/12, the risk events and the losses caused by these risk events continued to be investigated. Figure 9 shows the accumulating economic losses and delay time in the construction from 2012 to 2018. In the initial stage of construction, the loss is bigger than that in other stages, indicating that the construction risk mainly occurs during the initial stage. The project lost a total of 14.7 million CNY and was delayed by 36 months. In addition, one worker died, and seventeen workers were injured during the construction. Obviously, these losses are not acceptable for the construction enterprise, and it is appropriate to affirm that the risk level is I, which is associated with the assessment result of the FANPCE method. Therefore, the FANPCE method can be applied to assess the construction risk in subway station construction.

5. Method application process and limitation

The application process of the FANPCE model is shown in Figure 10. Risk factors and risk levels of subway station projects often change dynamically throughout the whole construction process; therefore, during the different stages, FANPCE model should be used repeatedly to obtain the accurate risk evaluations. According to the statistical and investigative data, there are mainly three methods of subway station construction methods, namely the open excavation method, covered excavation method, and semicovered and semiopen methods. The statistics of 178 subway stations are from official news and literature. 9 stations are under construction and 42 subway stations have been constructed by engineers from 9 investigating stations. Therefore, the network structure of risk factors shown in Figure 8 is applicable to a subway station which is constructed with the above three methods. If the subway station is built with other methods or as a part of other projects, the risk factors may differ from the risk factors in Figure 8. New risk factors for a particular site should be investigated, and the risk factors in the network structure should be replaced with new risk factors. The remaining steps are similar as described in this section.

6. Discussion

In this study, risk factors of subway station construction in China are identified, and a FANPCE model is developed to assess the construction risk. The model can be used for the risk management, so as to reduce the risk loss. In this study of risk factors. The study shows that, complicated underground pipelines, construction experience and safety consciousness have the highest weight among the rank I of risk factors, whereas out of limits, toxic content and geological disasters have the lowest weight among these factors. In other studies, construction safety is often the focus of risk assessment; the components of the support structure of the foundation pit becomes a risk factor in other studies (Chen & Song, 2012; Lan & Zhang, 2006; Li,
Du, Zhang, & Gao, 2009; Ying et al., 2016). Additionally, these risk factors are collected from other studies and lack the field risk investigation. In addition, numerous studies deeply investigate risk assessment methods, while the identification of risk factors is not fully considered (Dikmen & Birgonul, 2006). Based on the proposed construction project, the results imply that the construction risk rank of the Wu Lu Kou subway station is I. This indicates that there is a high probability of frequent losses caused by risk events. The result implies that, in response to the rank I risk, government authorities and construction parties should implement risk control measures to reduce the risk to acceptable or negligible levels and prepare or revise the risk warning and the emergency response plan. Therefore, a project manager should plan and implement resources for the project. For example, the results indicate that the weight of the safety consciousness of personnel is high. Therefore, some safety training or other measures should be implemented to enhance the safety consciousness of personnel. For example, when there is a high weight of the safety consciousness of personnel, safety training or other measures should be implemented to enhance the safety consciousness of personnel.

However, many mathematical calculations are employed in the model, so relevant mathematics knowledge is required for engineers. In future studies, mathematical calculations can be performed via computer programming. It should be noted that the network structure of risk factors is applicable to a subway station that is constructed by the open excavation method, covered excavation method and semicovered and semiopen methods in China. Risk factors and the identified weights in this study can be employed in the future research. The risk assessment for a subway station can be performed with this method. If the subway station is built by other methods, or at another stage of the project, or different construction risk is assessed in other studies, the risk factors and their weights may differ from those in this research. New risk factors for a particular site should be investigated, and the risk factors in the network structure should be replaced with the new risk factors.

Conclusions

In the construction of subway stations, effective risk identification and assessment should be performed to reduce the risk and ensure the safety of the construction site. In this study, twelve key risk factors of subway station construction were identified through literature review and questionnaires. The interdependencies among risk factors were represented through the network structure of ANP. The investigation results indicate that the complicated underground pipeline, limited construction experience and poor safety consciousness are weighted as highest risk factors for the studied subway station construction. Then, the weights matrix of single risk factors and interdependencies weights matrix were quantified by integrating the TFN into the ANP. Finally, the total risk rank of the studied project can be quantified through the synthesis of weight matrices with the synthetic operator of FCE. FANPCE method can be as an integration of the network analysis method, fuzzy set theory and FCE method to tackle uncertain and ambiguous risk assessment. In addition, a particular subway station was employed as a case study. The assessment results and the accident loss analysis verify the accuracy and applicability of the FANPCE model to a certain degree.

The advantages of FANPCE are concluded as: (1) the proposed method can be used as an operational tool. Engineers of subway station can consider the interactions of each factor and identify, assess and quantify risks of subway station construction through the proposed method; (2) risk factors can be identified with high risk weights; (3) The model can be applied to quantize and evaluate the risk level throughout the construction process, so as to control of construction risk.

The limitations and disadvantages of the method are concluded as: (1) 12 third-level risk factors of subway station construction may not be completely the same due to different construction environments and methods. Therefore, based on field risk identification, 12 third-level risk factors should be replaced with more exact risk factors and the number of risk factors should be changed; (2) as the number of projects increases, the size of the matrices increases, resulting in a higher number of calculations.

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Author contributions

Luyuan Wu conceived the study and were responsible for the design and development of the data analysis. Haibo Bai and Yuan Chao were responsible for data collection and analysis. Changyu Xu wrote the first draft of the article.

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### Abbreviations

**FTA**  – fault tree analysis;  
**FMCDM**  – Fuzzy multiple criteria decision making;  
**AHP**  – Analytic Hierarchy Process;  
**ANP**  – Analytic Network Process;  
**FCE**  – Fuzzy Comprehensive Evaluation;  
**FANPCE**  – Fuzzy Analytic Network Process Comprehensive Evaluation;  
**TLRF**  – Third Level Risk Factors;  
**FCM**  – Fuzzy Comparison Matrix;  
**FWM**  – Fuzzy Weight Matrix.

### Notations

#### Variables and functions

- \( l \) – lower bound of the fuzzy number;  
- \( m \) – intermediate value of a fuzzy number;  
- \( u \) – upper bound of the fuzzy number;  
- \( v_1, v_2, v_3, v_4 \) – final weight of risk level I, II, III, IV;  
- \( R_{(0)}{V_1}, R_{(0)}{V_2}, R_{(0)}{V_3}, R_{(0)}{V_4} \) – weights of each TLRF at risk level I, II, III, IV when taking the probability of generating risk, the loss degree and the controllability of the risk as criteria;  
- \( a_{ij} \) – weight of subblock \( i \) in super matrix \( W \);  
- \( \mu_F(x) \) – Degree of Membership Function.