Learning Anaphoricity and Antecedent Ranking Features for Coreference Resolution

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Abstract

We introduce a simple, non-linear mention-ranking model for coreference resolution that attempts to learn distinct feature representations for anaphoricity detection and antecedent ranking, which we encourage by pre-training on a pair of corresponding subtasks. Although we use only simple, unconjoined features, the model is able to learn useful representations, and we report the best overall score on the CoNLL 2012 English test set to date.

1 Introduction

One of the major challenges associated with resolving coreference is that in typical documents the number of mentions (syntactic units capable of referring or being referred to) that are non-anaphoric – that is, that are not coreferent with any previous mention – far exceeds the number of mentions that are anaphoric (Kummerfeld and Klein, 2013; Durrett and Klein, 2013). This preponderance of non-anaphoric mentions makes coreference resolution challenging, partly because many basic coreference features, such as those looking at head, number, or gender match fail to distinguish between truly coreferent pairs and the large number of matching but nonetheless non-coreferent pairs. Indeed, several authors have noted that it is difficult to obtain good performance on the coreference task using simple features (Lee et al., 2011; Fernandes et al., 2012; Durrett and Klein, 2013; Kummerfeld and Klein, 2013; Björkelund and Kuhn, 2014) and, as a result, state-of-the-art systems tend to use linear models with complicated feature conjunction schemes in order to capture more fine-grained interactions. While this approach has shown success, it is not obvious which additional feature conjunctions will lead to improved performance, which is problematic as systems attempt to scale with new data and features.

In this work, we propose a data-driven model for coreference that does not require pre-specifying any feature relationships. Inspired by recent work in learning representations for natural language tasks (Collobert et al., 2011), we explore neural network models which take only raw, unconjoined features as input, and attempt to learn intermediate representations automatically. In particular, the model we describe attempts to create independent feature representations useful for both detecting the anaphoricity of a mention (that is, whether or not a mention is anaphoric) and ranking the potential antecedents of an anaphoric mention. Adequately capturing anaphoricity information has long been thought to be an important aspect of the coreference task (see Ng (2004) and Section 7), since a strong non-anaphoric signal might, for instance, discourage the erroneous prediction of an antecedent for a non-anaphoric mention even in the presence of a misleading head match.

We furthermore attempt to encourage the learning of the desired feature representations by pre-training the model’s weights on two corresponding subtasks, namely, anaphoricity detection and antecedent ranking of known anaphoric mentions. Overall our best model has an absolute gain of almost 2 points in CoNLL score over a similar but linear mention-ranking model on the CoNLL 2012 English test set (Pradhan et al., 2012), and of over 1.5 points over the state-of-the-art coreference system. Moreover, unlike current state-of-the-art systems, our model does only local inference, and is therefore significantly simpler.

1.1 Problem Setting

We consider here the mention-ranking (or “mention-synchronous”) approach to coreference...
resolution (Denis and Baldridge, 2008; Bengtson and Roth, 2008; Rahman and Ng, 2009), which has been adopted by several recent coreference systems (Durrett and Klein, 2013; Chang et al., 2013). Such systems aim to identify whether a mention is coreferent with an antecedent mention, or whether it is instead non-anaphoric (the first mention in the document referring to a particular entity). This is accomplished by assigning a score to the mention’s potential antecedents as well as to the possibility that it is non-anaphoric, and then predicting the greatest scoring option. We furthermore assume the more realistic “system mention” setting, where it is not known a priori which mentions in a document participate in coreference clusters, and so (all) mentions must be automatically extracted, typically with the aid of automatically detected parse trees.

Formally, we denote the set of automatically detected mentions in a document by \(\mathcal{X}\). For a mention \(x \in \mathcal{X}\), let \(\mathcal{A}(x)\) denote the set of mentions appearing before \(x\); we refer to this set as \(x\)’s potential antecedents. Additionally let the symbol \(\epsilon\) denote the empty antecedent, to which we will view \(x\) as referring when \(x\) is non-anaphoric.\(^1\) Denoting the set \(\mathcal{A}(x) \cup \{\epsilon\}\) by \(\mathcal{Y}(x)\), a mention-ranking model defines a scoring function \(s(x, y) : \mathcal{X} \times \mathcal{Y} \to \mathbb{R}\), and predicts the antecedent of \(x\) to be \(y^* = \arg \max_{y \in \mathcal{Y}(x)} s(x, y)\).

It is common to be quite liberal when extracting mentions, taking, essentially, every noun phrase or pronoun to be a candidate mention, so as not to prematurely discard those that might be coreferent (Lee et al., 2011; Fernandes et al., 2012; Chang et al., 2012; Durrett and Klein, 2013). For instance, the Berkeley Coreference System (herein BCS) (Durrett and Klein, 2013), which we use for mention extraction in our experiments, recovers approximately 96.4% of the truly anaphoric mentions in the CoNLL 2012 training set, with an almost 3.5:1 ratio of non-anaphoric mentions to anaphoric mentions among the extracted mentions.

2 Mention Ranking Models

The structural simplicity of the mention-ranking framework puts much of the burden on the scoring function \(s(x, y)\). We begin by considering mention-ranking systems using linear scoring functions. In the next section, we will extend these models to operate over learned non-linear representations.

Linear mention-ranking models generally utilize the following scoring function

\[
s_{lin}(x, y) \triangleq \mathbf{w}^T \phi(x, y)
\]

where \(\phi : \mathcal{X} \times \mathcal{Y} \to \mathbb{R}^d\) is a pairwise feature function defined on a mention and a potential antecedent, and \(\mathbf{w}\) is a learned parameter vector.

To add additional flexibility to the model, linear mention ranking models may duplicate individual features in \(\phi\), with one version being used when predicting an antecedent for \(x\), and another when predicting that \(x\) is non-anaphoric (Durrett and Klein, 2013). Such a scheme effectively gives rise to the following piecewise scoring function

\[
s_{lin+}(x, y) \triangleq \begin{cases} 
\mathbf{u}^T \phi_a(x) & \text{if } y \neq \epsilon \\
\mathbf{v}^T \phi_p(x) & \text{if } y = \epsilon
\end{cases}
\]

where \(\phi_a : \mathcal{X} \to \mathbb{R}^{d_a}\) is a feature function defined on a mention and its context, \(\phi_p : \mathcal{X} \times \mathcal{Y} \to \mathbb{R}^{d_p}\) is a pairwise feature function defined on a mention and a potential antecedent, and parameters \(\mathbf{u}\) and \(\mathbf{v}\) replace \(\mathbf{w}\). Above, we have made an explicit distinction between pairwise features (\(\phi_p\)) and those strictly on \(x\) and its context (\(\phi_a\)), and moreover assumed that our features need not examine potential antecedents when predicting \(y = \epsilon\).

We refer to the basic, unconjoined features used for \(\phi_a\) and \(\phi_p\) as raw features. Figure 2 shows two versions of these features, a base set BASIC and an extended set BASIC+. The BASIC set are the raw features used in BCS, and BASIC+ includes additional raw features used in other recent coreference systems. For instance, BASIC+ additionally includes features suggested by Recasens et al. (2013) to be useful for anaphorically, such as the number of a mention, its named entity status, and its animacy, as well as number and gender information. We additionally include binomial head features, which are used in many well-performing systems (for instance, that of Fernandes et al. (2012)).

2.1 Problems with Raw Features

Many authors have observed that, taken individually, raw features tend to not be particularly predictive for the coreference task. We examine this phenomenon empirically in Figure 1. These

\(^1\)We make this stipulation for modeling convenience; it is not intended to reflect any linguistic fact.
Figure 1: Two histograms illustrating the predictive ability of raw (unconjoined) features per feature occurrence: (top) mention-context features from \( \phi_a \) as independent predictors of anaphoricity \((y \neq \epsilon)\), and (bottom) antecedent-mention features from \( \phi_p \) as independent predictors of coreferent mentions. Very few raw features are strong indicators of either anaphoricity or an antecedent match. Data taken from the CoNLL development set.

To address this issue, state-of-the-art mention-ranking systems often rely on manual or otherwise induced conjunction schemes to capture specific feature interactions. Durrett and Klein (2013), for instance, conjoin all raw features in \( \phi_p \) with the type of the current mention and antecedent. For these purposes, the type of a mention is either “nominal”, “proper”, or a canonicalization of the pronoun if it is a pronominal mention. Fernandes et al. (2012) and Björkelund and Kuhn (2014) use an automatic but complicated scheme to induce conjunctions by first extracting feature templates from a separately trained decision tree, and then doing greedy forward selection among the templates. These conjunctions add some non-linearity to the scoring function while still maintaining a tractable, though large, feature set.

## 3 Learning Features for Ranking

As an alternative to the aforementioned feature conjunction schemes, we consider learning feature representations in order to better capture relevant aspects of the task. Representation learning affords the model more flexibility in exploiting feature interactions, although it can make the underlying training problem more difficult.

### 3.1 Model

We use a neural network to define our model as an extension to the mention-ranking model introduced in Section 2. We consider in particular the scoring function:

\[
s(x, y) \triangleq \begin{cases} 
  u^T g \left( \begin{bmatrix} h_a(x) \\ h_p(x, y) \end{bmatrix} \right) + u_0 & \text{if } y \neq \epsilon \\
  v^T h_a(x) + v_0 & \text{if } y = \epsilon
\end{cases}
\]
where $h_a$ and $h_p$ are feature representations, non-linear functions of the features $\phi_a$ and $\phi_p$ (respectively), and $g$ is a function of these representations. In particular, we define

$$h_a(x) \triangleq \tanh(W_a \phi_a(x) + b_a) \quad h_p(x, y) \triangleq \tanh(W_p \phi_p(x, y) + b_p),$$

and we take $g$ to either be the identity function, in which case the above model is analogous to $s_{lin+}$ but defined over non-linear feature representations, or to be an additional hidden layer: $g(\begin{pmatrix} h_a(x) \\ h_p(x, y) \end{pmatrix}) = \tanh(W \begin{pmatrix} h_a(x) \\ h_p(x, y) \end{pmatrix} + b)$. For ease of exposition, we will refer to these two settings of $g$ as $g_1$ and $g_2$ (respectively) in what follows. As we will see below, both settings lead to comparable performance, but to a different error distribution.

In either case, by defining the functions $h_a$ and $h_p$, we allow the model to learn representations of the input features $\phi_a$ and $\phi_p$. The benefit of the added non-linearities is that, in theory, it is no longer necessary to explicitly specify feature conjunctions, since the model may learn them automatically if necessary. Accordingly, for this model we use only $\phi_a$ and $\phi_p$ consisting of the raw features in Figure 2 without conjunctions. Any interaction between these features must be learned by the feature representations $h_p$ and $h_a$.

### 3.2 Training

We can directly train our model using back-propagation. To specify the training problem, we first define notation for the training objective.

Define the set $C(x)$ to contain just the mentions in $A(x)$ that are coreferent with $x$. We then define

$$C'(x) = \begin{cases} C(x) & \text{if } x \text{ is anaphoric} \\ \{\epsilon\} & \text{otherwise} \end{cases}$$

Finally, let $y_n^* = \arg \max_{y \in C'(x_n)} s(x_n, y)$ be the highest scoring correct antecedent of $x_n$, which may be $\epsilon$. (Thus, following recent work (Yu and Joachims, 2009; Fernandes et al., 2012; Chang et al., 2013; Durrett and Klein, 2013), we view each mention as having a “latent antecedent”.)

We train to minimize the regularized, slack-rescaled, latent-variable loss \(^3\) given by:

$$L(\theta) = \sum_{n=1}^N \max_{\hat{y} \in C'(x_n)} \Delta(x_n, \hat{y})(1 + s(x_n, \hat{y}) - s(x_n, y_n^*)) + \lambda ||\theta||_1,$$

where $\Delta$ is a mistake-specific cost function, which is 0 when $\hat{y} \in C'(x_n)$. Above, we use $\theta$ to refer to the full set of parameters \{\(W, u, v, W_a, W_p, b_a, b_p\)\}. For experiments, we define $\Delta$ to take on different costs for the three kinds of mistakes possible in a coreference task, as follows:

$$\Delta(x, \hat{y}) = \begin{cases} \alpha_1 & \text{if } \hat{y} \neq \epsilon \land \epsilon \in C'(x) \\ \alpha_2 & \text{if } \hat{y} = \epsilon \land \epsilon \notin C'(x) \\ \alpha_3 & \text{if } \hat{y} \neq \epsilon \land \hat{y} \notin C'(x) \end{cases}.$$

The $\alpha_i$ determine the trade-off between these mistakes (and thus precision and recall). Adopting the terminology of BCS, we refer to these mistakes as “false link” (FL), “false new” (FN), and “wrong link” (WL), respectively.

### 4 Representations from Subtasks

While we could train our full model directly, it is known to be difficult to train high performing non-convex neural-network models from a random initialization (Erhan et al., 2010). In order to overcome the problems associated with training from this setting, and to learn feature representations useful for the full coreference task, we pretrain subparts of the model on the subtasks targeting the desired feature representations. We then train the entire model on the full coreference task (from the pre-trained initializations). As we will see, the pre-training scheme outlined below helps the model achieve improved performance.

The proposed pre-training scheme involves learning the parameters associated with $h_a$ and $h_p$ using two natural subtasks: anaphoricity detection and antecedent ranking. In particular, we (1) train $h_a$ on the task of predicting whether a particular mention is anaphoric or not, and (2) train $h_p$ on the task of predicting the antecedent of mentions known to be anaphoric.

#### 4.1 Anaphoricity Detection

For the first subtask we attempt to predict whether a mention is anaphoric or not based only on its

\(^3\)Previous work divides between log-loss and margin loss. We use the latter because gradient updates (within backprop) for the non-probabilistic objectives only involve terms relating to $\hat{y}$ and $y_n^*$, and are therefore faster.
Table 1: Performance of the two subtasks on the CoNLL 2012 development set by feature set and model type. “Conj.” indicates whether conjunctions are used. The linear anaphoric system is an SVM (LibLinear implementation (Fan et al., 2008)), and the linear antecedent system is a linear model with the margin-based objective.

| Feat. (Conj.) | Model | Anaphoric | P | R | F₁ | Ante Acc. |
|---------------|-------|------------|---|---|----|----------|
| BASIC (N)     | Lin.  | 74.15      | 74.20 | 74.18 | 69.10 | |
| BASIC (Y)     | Lin.  | 73.98      | 75.04 | 74.51 | 79.76 | |
| BASIC (N)     | NN    | 75.30      | 75.36 | 75.33 | 81.65 | |
| BASIC+ (N)    | Lin.  | 74.14      | 74.71 | 74.43 | 74.02 | |
| BASIC+ (Y)    | Lin.  | 74.24      | 75.39 | 74.81 | 80.44 | |
| BASIC+ (N)    | NN    | 75.84      | 76.02 | 75.93 | 82.86 | |

Figure 3: Visualization of the representation matrix $W_p$. A subset of the raw features were manually grouped into five classes indicating: full lexical match $[F]$, head match $[H]$, mention/sentence distance $[D]$ (near versus far), gender/number match $[G]$, and type $[P]$ (pronoun versus other). The heat map illustrates 10-columns of $W_p$, as a weighted combination of these classes, roughly illustrating the combination of raw features required for this dimension of the representation.

4.3 Subtask Performance

As a preliminary experiment, we train models for these two subtasks using both the BASIC and BASIC+ raw features. Table 1 shows the results. For the first subtask, experiments look at the precision, recall, and $F_1$ score of predicting anaphoric mentions on the CoNLL 2012 development set. As a baseline we use an L1-regularized SVM implemented using LibLinear (Fan et al., 2008), both using raw features and using features conjoined according to the BCS scheme. For the second subtask, experiments look at the accuracy of the model in predicting the correct antecedent on known anaphoric mentions. As a baseline we use a linear mention ranking model, with and without

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4. While performance on this subtask can in fact be improved further by looking at previous mentions, features learned in this way led to inferior performance on the full task.

5. Note that singleton detection is slightly different from anaphoricity detection, since a mention can be non-anaphoric but not a singleton if it is the first mention in a cluster.
conjunctions, trained using the same margin-based loss.

In both subtasks, the neural network model performs quite well, significantly better than the unconjoined baselines and better than the model trained with manually conjoined features. We provide a visual representation of the antecedent ranking features learned in Figure 3. While the improved subtask performance does not imply better performance on the full coreference task, it shows that model can learn useful feature representations with only raw input features.

5 Coreference Experiments

Our experiments examine performance as compared with other coreference systems, as well as the effect of features, pre-training, and model architecture. We also perform a qualitative comparison of our model with the analogous linear model on some challenging non-anaphoric cases.

5.1 Methods

All experiments use the CoNLL 2012 English dataset (Pradhan et al., 2012), which is based on the OntoNotes corpus (Hovy et al., 2006). The data set contains 3,493 documents consisting of 1.6 million words. We use the standard experimental split with the training set containing 2,802 documents and 156K annotated mentions, the development set containing 343 documents and 19K annotated mentions, and the test set containing 348 documents and 20K annotated mentions. For all experiments, we use BCS (Durrett and Klein, 2013) to extract system mentions and to compute some of the features.

For training, we minimize the loss described above using the composite mirror descent AdaGrad update (Duchi et al., 2011) with document sized mini-batches.\(^6\) We tuned the AdaGrad learning rate and regularization parameters using a grid search over possible learning rates \(\eta \in \{0.001, 0.002, 0.01, 0.02, 0.1, 0.2\}\) and over regularization parameters \(\lambda \in \{10^{-6}, \ldots, 10^{-1}\}\). For the full coreference task, we use a different learning rate for the pre-trained weights and for the second-layer weights, using \(\eta_1 = 0.1\) and \(\eta_2 = 0.001\), respectively, and \(\lambda = 10^{-6}\). When initializing weight-matrices that were not pre-trained we used the sparse initialization technique proposed by Sutskever et al. (2013). For all experiments we use the cost-weights \(\alpha = (0.5, 1.2, 1)\) in defining \(\Delta\).

For the anaphoricity representations the matrix dimensions used are \(W_\alpha \in \mathbb{R}^{128 \times d_\alpha}\), and for the pairwise representations the matrix dimensions used are \(W_p \in \mathbb{R}^{700 \times d_p}\). In the \(g_\alpha\) model, the outer matrix dimensions are \(W \in \mathbb{R}^{128 \times (d_p + d_\alpha)}\). With the BASIC+ features, \(d_p\) and \(d_\alpha\) come out to be slightly less than \(10^6\) and \(10^4\), respectively, with bilexical head features accounting for the vast majority of \(d_p\).\(^7\) We tuned all hyper-parameters (as well as those of baseline systems) on the development set.

We use the CoNLL 2012 scoring script v8.01\(^8\) (Pradhan et al., 2014; Luo et al., 2014), which scores based on 3 metrics, including MUC (Vilain et al., 1995), CEAF\(_e\) (Luo, 2005), and B\(^3\) (Bagga and Baldwin, 1998), as well as the CoNLL score, which is the arithmetic mean of the 3 metrics.

Code implementing our models is available at https://github.com/swiseman/nn_coref. The system trains in time comparable to that of linear systems, mainly because we use only raw features and sparse margin-based gradient updates.

5.2 Results

Our main results are shown in Table 2. This table compares the performance of our system with the performance reported by several other state-of-the-art systems on the CoNLL 2012 English coreference test set. Our full models achieve the best \(F_1\) score across two of the three metrics and have the best aggregate (CoNLL) score, with an improvement of over 1.5 points over the best reported result, and of almost 2 points over the best mention-ranking system. Our \(F_1\) improvements on all three metrics are significant \((p < 0.05\) under the bootstrap resample test (Koehn, 2004)) as compared with both Björkelund and Kuhn (2014), and Durrett and Klein (2014), the two most recent, state-of-the-art systems.

Since our full models use some additional raw features (although an order of magnitude fewer total features than the comparable conjunction-

\(^6\)In preliminary experiments we also used Nesterov’s accelerated gradient (Nesterov, 1983), but found AdaGrad to perform better.

\(^7\)Note that the BCS conjunction scheme, for instance, applied to our raw features gives a \(d_p\) and \(d_\alpha\) that are over an order of magnitude larger.

\(^8\)http://conll.github.io/reference-coreference-scorers/
based linear model), we are interested in what part of the improvement in performance comes from features rather than modeling power. Table 3 compares the full model to BCS, a system effectively using the \( s_{\text{lin+}} \) scoring function together with a manual conjunction scheme, on both BASIC and BASIC+ features. While our models outperform BCS in both cases, we see that as we add more features (as in the BASIC+ set), the performance gap between our model and the linear system becomes even more pronounced.

We may also wonder whether the architecture represented by our scoring function, where the intermediate representations \( h_a \) and \( h_p \) are separated in the first layer, is necessary for these results. We accordingly compare with the fully connected versions of these two models (which are equivalent to 1 and 2 layer multi-layer perceptrons) using the BASIC+ features in Table 4. There, we also evaluate the effect of pre-training on these models by comparing with the results of training from a random initialization. We see that while even randomly initialized models are capable of excellent performance, pre-training is beneficial, especially for \( g_1 \).

### Table 2: Results on CoNLL 2012 English test set. We compare against recent state-of-the-art systems, including (in order) Durrett and Klein (2013), Ma et al. (2014), Björklund and Kuhn (2014), and Durrett and Klein (2014) (rescored with the v8.01 scorer). \( F_1 \) gains are significant \((p < 0.05\) under the bootstrap resample test (Koehn, 2004)) compared with both B&K and D&K for all metrics.

| System                  | MUC P | MUC R | MUC F1 | B^3 P | B^3 R | B^3 F1 | CEAF_e P | CEAF_e R | CEAF_e F1 | CoNLL |
|-------------------------|-------|-------|--------|-------|-------|--------|----------|----------|----------|-------|
| BCS (2013)              | 74.89 | 67.17 | 70.82  | 64.26 | 53.09 | 58.14  | 58.12    | 52.67    | 55.27    | 61.41 |
| Prune&Score (2014)      | 81.03 | 66.16 | **72.84** | 66.9  | 51.10 | 57.94  | 68.75    | 44.34    | 53.91    | 61.56 |
| B&K (2014)              | 74.3  | 67.46 | 70.72  | 62.71 | 54.96 | 58.58  | 59.54    | 52.27    | 55.61    | 61.63 |
| D&K (2014)              | 72.73 | 69.98 | 71.33  | 61.18 | 56.60 | 58.80  | 56.20    | 54.31    | 55.24    | 61.79 |
| This work \((g_2)\)     | 76.96 | 68.10 | 72.26  | 66.90 | 54.12 | 59.84  | 59.02    | 53.34    | 56.03    | 62.71 |
| This work \((g_1)\)     | 73.23 | 69.31 | 72.60  | 66.67 | 55.83 | 60.52  | 59.41    | 54.88    | 57.05    | 63.39 |

Table 3: \( F_1 \) performance comparison between state-of-the-art linear mention-ranking model (Durrett and Klein, 2013) and our full models on CoNLL 2012 development set for different feature sets.

| Model | Features | MUC | B^3 | CEAF_e | CoNLL |
|-------|----------|-----|-----|--------|-------|
| Lin.  | \((g_2)\) BASIC | 70.44 | 59.10 | 55.57 | 61.71 |
| NN    | \((g_1)\) | 71.59 | 60.56 | 57.45 | 63.20 |
| Lin.  | \((g_2)\) BASIC+ | 72.68 | 61.70 | 58.32 | 64.23 |
| NN    | \((g_1)\) | 72.74 | 61.77 | 58.63 | 64.38 |

| Model | MUC | B^3 | CEAF_e | CoNLL |
|-------|-----|-----|--------|-------|
| Fully Conn. 1 Layer | 71.80 | 60.93 | 57.51 | 63.41 |
| Fully Conn. 2 Layer | 71.77 | 60.84 | 57.05 | 63.22 |
| \( g_1 + RI \) | 71.92 | 61.06 | 57.59 | 63.52 |
| \( g_1 + PT \) | 72.74 | 61.77 | 58.63 | 64.38 |
| \( g_2 + RI \) | 72.31 | 61.79 | 58.06 | 64.05 |
| \( g_2 + PT \) | 72.68 | 61.70 | 58.32 | 64.23 |

Table 4: Comparison of performance (in \( F_1 \) score) of various models on CoNLL 2012 development set using BASIC+ features. “PT” and “RI” refer to pretraining and random initialization respectively. “Fully Conn.” refers to baseline fully connected networks. See text for further model descriptions.

### 6 Discussion

We attempt to gain insight into our model’s errors using using two different error breakdowns. In Table 5 we show the errors as reported by the analysis tool of Kummerfeld and Klein (2013). In Table 6 we show a more fine-grained breakdown inspired by a similar analysis in Durrett and Klein (2013). In the latter table, we categorize the errors made by our system on the CoNLL 2012 development data in terms of (1) whether or not the mention has a head match with a previously occurring mention in the document, unless it is a pronominal mention, which we treat separately, (2) in terms of the status of the mention in the gold clustering, namely, singleton, first-in-cluster, or anaphoric, and (3) in terms of the type of error made (which, as discussed in Section 3, are one of FL, FN, and WL).

We note that the two models have slightly different error profiles, with \( g_1 \) being slightly better at recall and \( g_2 \) being slightly better at precision. Indeed, we see from Table 6 that the two models make a comparable number of total errors (\( g_1 \) makes only 17 fewer errors overall). The increased precision of the \( g_2 \) model is presumably due to the second layer around \( h_a \) and \( h_p \) in \( g_2 \) allowing for antecedent evidence to interact with anaphoricity.
Table 5: Absolute error counts from the coreference analysis tool of Kummerfeld and Klein (2013). The upper row sets up the precision and the lower to the recall of the coreference clusters produced by the model.

| Error Type            | BCS | NN (g₁) | NN (g₂) |
|-----------------------|-----|---------|---------|
| Conflated Entities    | 1603| 1434    | 1371    |
| Extra Mention         | 651 | 568     | 529     |
| Extra Entity          | 655 | 623     | 561     |
| Divided Entity        | 1989| 1837    | 1835    |
| Missing Mention       | 1004| 997     | 1005    |
| Missing Entity        | 1070| 1026    | 1114    |

Table 6: Errors made by NN (g₁) (top) and NN (g₂) (bottom) on CoNLL 2012 English development data. Rows correspond to (1) mentions with a (previous) head match (HM), that is, mentions \( x \) such that \( \mathcal{A}(x) \) contains another mention with the same head word, (2) with no previous head match (no HM), and (3) to pronominal mentions, respectively. The 3 column groups correspond to singleton, first-in-cluster, and anaphoric mentions (resp.), as determined by the gold clustering, with the number and type of errors on the left and the total number of mentions in the category (#) on the right.

| NN (g₁) | Singleton | 1ˢᵗ in clust. | Anaphoric |
|---------|-----------|---------------|-----------|
|         | FL       | #             | FL       | #         | FN + WL | #             |
| HM      | 817      | 8.2K          | 147      | 0.8K     | 700 + 318 | 4.7K          |
| No HM   | 86       | 19.8K         | 41       | 2.4K     | 677 + 59  | 1.0K          |
| Pron.   | 948      | 2.6K          | 257      | 0.5K     | 434 + 875 | 7.3K          |

| NN (g₂) | Singleton | 1ˢᵗ in clust. | Anaphoric |
|---------|-----------|---------------|-----------|
|         | FL       | #             | FL       | #         | FN + WL | #             |
| HM      | 770      | 8.2K          | 130      | 0.8K     | 803 + 306 | 4.7K          |
| No HM   | 73       | 19.8K         | 39       | 2.4K     | 699 + 52  | 1.0K          |
| Pron.   | 896      | 2.6K          | 249      | 0.5K     | 456 + 869 | 7.3K          |

Table 6 also gives a sense of where coreference systems such as ours need to improve. It is first important to note that the case of resolving an anaphoric mention that has no previous head matches (e.g., identifying that “the team” and “the New York Giants” are coreferent), which is often taken to be one of the major challenges facing coreference systems because it presumably requires semantic information, is not the largest source of errors. In fact, we see from Table 6 (second row, third column in both sub-tables) that while these cases do indeed account for a substantial percentage of errors, we make hundreds more errors predicting singleton pronominal mentions to be anaphoric (in the case of \( g₁ \)) and on incorrectly linking anaphoric pronominal mentions (in the case of \( g₂ \)). Further analysis indicates that these errors are almost entirely related to incorrectly linking pleonastic pronouns, such as “it” or “you,” and that moreover the incorrectly predicted antecedent for these pleonastic pronouns is almost always (another instance of) the same pronoun.

That these pleonastic cases are so problematic is interesting when considered against the backdrop of the inference strategies typically employed by coreference systems, which we briefly mention here but discuss more fully in the next section. Currently, coreference systems divide be-

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**Figure 4:** Example mentions \( x \) that were correctly marked non-anaphoric by \( g₂ \), but incorrectly marked anaphoric with \( y \) as an antecedent by the B\( g_{1}\) + linear model. These examples highlight the difficult case where there is a spurious head-match between non-coreferent pairs. See text for further details.

"company-company" head match is often misleading, and, in general, distance features may also rule out head matches. Note that while these features on their own may be more or less correlated with a mention being non-anaphoric, the model learns to combine them in a predictive way.

### 6.1 Further Improving Coreference Systems

Table 6 also gives a sense of where coreference systems such as ours need to improve. It is first important to note that the case of resolving an anaphoric mention that has no previous head matches (e.g., identifying that “the team” and “the New York Giants” are coreferent), which is often taken to be one of the major challenges facing coreference systems because it presumably requires semantic information, is not the largest source of errors. In fact, we see from Table 6 (second row, third column in both sub-tables) that while these cases do indeed account for a substantial percentage of errors, we make hundreds more errors predicting singleton pronominal mentions to be anaphoric (in the case of \( g₁ \)) and on incorrectly linking anaphoric pronominal mentions (in the case of \( g₂ \)). Further analysis indicates that these errors are almost entirely related to incorrectly linking pleonastic pronouns, such as “it” or “you,” and that moreover the incorrectly predicted antecedent for these pleonastic pronouns is almost always (another instance of) the same pronoun.

That these pleonastic cases are so problematic is interesting when considered against the backdrop of the inference strategies typically employed by coreference systems, which we briefly mention here but discuss more fully in the next section. Currently, coreference systems divide be-

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| Error Type | BCS | NN (g₁) | NN (g₂) |
|------------|-----|---------|---------|
| Conflated Entities | 1603 | 1434 | 1371 |
| Extra Mention | 651 | 568 | 529 |
| Extra Entity | 655 | 623 | 561 |
| Divided Entity | 1989 | 1837 | 1835 |
| Missing Mention | 1004 | 997 | 1005 |
| Missing Entity | 1070 | 1026 | 1114 |

Table 5: Absolute error counts from the coreference analysis tool of Kummerfeld and Klein (2013). The upper row sets up the precision and the lower to the recall of the coreference clusters produced by the model.

| NN (g₁) | Singleton | 1ˢᵗ in clust. | Anaphoric |
|---------|-----------|---------------|-----------|
|         | FL       | #             | FL       | #         | FN + WL | #             |
| HM      | 817      | 8.2K          | 147      | 0.8K     | 700 + 318 | 4.7K          |
| No HM   | 86       | 19.8K         | 41       | 2.4K     | 677 + 59  | 1.0K          |
| Pron.   | 948      | 2.6K          | 257      | 0.5K     | 434 + 875 | 7.3K          |

| NN (g₂) | Singleton | 1ˢᵗ in clust. | Anaphoric |
|---------|-----------|---------------|-----------|
|         | FL       | #             | FL       | #         | FN + WL | #             |
| HM      | 770      | 8.2K          | 130      | 0.8K     | 803 + 306 | 4.7K          |
| No HM   | 73       | 19.8K         | 39       | 2.4K     | 699 + 52  | 1.0K          |
| Pron.   | 896      | 2.6K          | 249      | 0.5K     | 456 + 869 | 7.3K          |
between those using “local” models, which choose antecedents for potentially anaphoric mentions independently of each other, and “non-local” models, which make predictions that take into account predictions made for previous mentions, and perhaps even attempt to jointly predict all mentions in a document. While our model is entirely local, other recent high performing systems, such as that of Björkelund and Kuhn (2014), are not. One might suspect, then, that “non-local” inference might allow us to capture the fact that, for instance, a cluster of coreferent mentions should generally not consist solely of pronouns, and thereby avoid predicting (identical) pronominal antecedents for pleonastic pronouns.

As it turns out, however, almost 30% of the anaphoric pronominal mentions in the CoNLL development data participate in pronoun-only clusters (primarily in the context of broadcast or telephone conversations), which suggests that such a “non-local” rule may not be particularly useful, though further experiments are required. It is also worth noting that a suitably modified loss function may also be able to prevent excessive pronoun-pronoun linking, even in a local model.

7 Related Work

There is a voluminous literature on machine learning approaches to coreference resolution, effectively beginning with Soon et al. (2001). The recent introduction of the CoNLL datasets (Pradhan et al., 2012) has spurred research that takes advantage of more fine-grained features and richer models (Björkelund and Farkas, 2012; Chang et al., 2012; Durrett and Klein, 2013; Chang et al., 2013; Björkelund and Kuhn, 2014; Ma et al., 2014). Of these approaches, our model is related to the mention-ranking approaches (Bengtson and Roth, 2008; Denis and Baldridge, 2008; Rahman and Ng, 2009; Durrett and Klein, 2013; Chang et al., 2013), as opposed to those that focus on non-local, structured prediction (McCullam and Wellner, 2003; Cullotta et al., 2006; Haghhighi and Klein, 2010; Fernandes et al., 2012; Stoyanov and Eisner, 2012; Björkelund and Farkas, 2012; Wick et al., 2012; Björkelund and Kuhn, 2014; Durrett and Klein, 2014).

In motivation, our work is most similar to that of Ng (2004), who notes that anaphoricity information is useful within the broader coreference task, and who accordingly attempts to “globally” optimize performance based on this information, as well as that of Denis et al. (2007), who do joint decoding of anaphoricity and coreference predictions using ILP. Both of these works are taken to contrast with the more popular approach of doing an initial non-anaphoric pruning step (Ng and Cardie, 2002; Rahman and Ng, 2009; Recasens et al., 2013; Lee et al., 2013). In contrast, we jointly learn non-linear functions of anaphoricity and antecedent features, rather than tune a threshold, or jointly decode based on independently trained classifiers (as in Denis et al. (2007)). In a similar vein, several authors have also proposed using the output of an anaphoricity classifier as a feature in a downstream coreference system (Ng, 2004; Bengtson and Roth, 2008). In our framework we (re)learn features jointly with the full task, after a pre-training scheme that targets anaphoricity as well antecedent representations.

There has also been some work on automatically inducing feature conjunctions for use in coreference systems (Fernandes et al., 2012; Lassalle and Denis, 2013), though the approach we present here is somewhat simpler, and unlike that of Lassalle and Denis (2013) is designed for use on system rather than gold mentions.

There has been much interest recently in using neural networks for classic natural language tasks such as tagging and semantic role labeling Collobert et al. (2011), sentiment analysis (Socher et al., 2011; Socher et al., 2012), prepositional phrase attachment (Belinkov et al., 2014) among others. These systems often use some form of pre-training for initialization, often word-embeddings learned from external tasks. However, there has been little work of this form for coreference resolution.

8 Conclusion

We have presented a simple, local model capable of learning feature representations useful for coreference-related subtasks, and of thereby achieving state-of-the-art performance. Because our approach automatically learns intermediate representations given raw features, directions for further research might alternately explore including additional (perhaps semantic) raw features, as well as developing loss functions that further discourage learning representations that allow for common errors (such as those involving pleonastic pronouns).
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