Three-disk microswimmer in a supported fluid membrane

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A model of three-disk micromachine swimming in a quasi two-dimensional supported membrane is proposed. We calculate the average swimming velocity as a function of the disk size and the arm length. Due to the presence of the hydrodynamic screening length in the quasi two-dimensional fluid, the geometric factor appearing in the average velocity exhibits three different asymptotic behaviors depending on the microswimmer size and the hydrodynamic screening length. This is in sharp contrast to a microswimmer in a three-dimensional bulk fluid that shows only a single scaling behavior. We also find that the maximum velocity is obtained when the disks are equal-sized, whereas it is minimized when the average arm lengths are identical. The intrinsic drag of the disks on the substrate does not alter the scaling behaviors of the geometric factor.

I. INTRODUCTION

Biological membranes are composed of lipid molecules and various types of proteins which can move laterally due to the membrane fluidity. Hence biomembranes play important roles in various life processes, such as the transportation of materials or the reaction between chemical species. While some proteins are subjected to thermal agitations of lipid molecules and undergo passive Brownian motions, there is also a large number of active proteins which cyclically change their conformations. For instance, with a supply of adenosine triphosphate (ATP), some proteins act as ion pumps by changing their structural conformations in order to allow materials to pass through the membranes. In general, such cyclic motions of proteins can lead to their active locomotion under certain conditions rather than just a passive motion.

By transforming chemical energy into mechanical work, microswimmers change their shape and move in viscous environments. Over the length scale of microswimmers, the fluid forces acting on them are governed by the effect of viscous dissipation. According to Purcell’s scallop theorem, time-reversal body motion cannot be used for locomotion in a Newtonian fluid. As one of the simplest models exhibiting broken time-reversal symmetry in a three-dimensional (3D) fluid, Najafi and Golestanian proposed a three-sphere swimmer, in which three in-line spheres are linked by variable elastic springs. In their model, the natural lengths of the springs depend on the discrete states that are cyclically switched. They also performed a microscopic dynamical simulation, where the lipid bilayer structure of the membrane is resolved and the solvent effects are included by multiparticle collision dynamics. For quasi-2D fluids, there exists a hydrodynamic screening length which distinguishes 2D and 3D hydrodynamic interactions.

In this paper, we present a systematic and also analytical investigation on the locomotion of a 2D microswimmer immersed in a supported fluid membrane, i.e., a lipid bilayer membrane located on a solid substrate. For supported membranes, the membrane-substrate distance is usually not large, and such a direct contact leads to a frictional coupling between the membrane and the solid support. Our swimmer consists of three thin rigid disks (rather than spheres) connected by two arms or springs which can undergo prescribed cyclic motions. We employ the 2D mobility and the coupling mobility that take into account the hydrodynamic interactions mediated by the quasi-2D fluid in the presence of the substrate. We analytically obtain the average velocity of such a three-disk micromachine as a function of the disk and arm sizes. Due to the presence of the hydrodynamic screening length associated with the quasi-2D fluid model, the geometric factor in the average velocity exhibits various asymptotic size dependencies, which is in sharp contrast to a microswimmer in a 3D bulk fluid.
In the above, respectively, \( (m/s) \) and \( \text{croswimmers in Sec. V. Finally, the summary of our work tor appearing in the average velocity. We also examine \( \text{croswimmer in a supported membrane. In Sec. IV, we discuss the motion of a 2D three-disk mi-

a quasi-2D fluid describing a supported membrane. In such a situation, the friction parameter in Eq. (1) can be identified as \( \lambda = \eta / h \), provided that \( h \) is small enough [23].

Solving the above quasi-2D hydrodynamic equations, one can obtain the translational mobility coefficient \( \mu \) of a rigid disk that is defined by \( V = \mu F \), where \( V \) is the disk velocity and \( F \) is a driving force. By using the no-slip boundary condition, the resulting expression becomes [23, 25]

\[
\mu(a) = \frac{1}{4\pi \eta} \left( \frac{(\kappa a)^2}{4} + \frac{\kappa a K_1(\kappa a)}{K_0(\kappa a)} \right)^{-1},
\]

where \( a \) is the disk radius, \( \kappa = \sqrt{\lambda / \eta} \), and \( K_0 \) and \( K_1 \) are modified Bessel functions of the second kind, order zero and one, respectively. Physically, \( \kappa^{-1} \) represents the hydrodynamic screening length beyond which the 2D hydrodynamic interaction becomes irrelevant. Notice that \( \kappa^{-1} \) diverges as \( \lambda \to 0 \), which alludes the Stokes paradox in a pure 2D fluid [23, 24]. The effect of intrinsic drag of the disk on the substrate will be discussed later in the final section.

For \( \kappa a \ll 1 \), the above disk mobility asymptotically behaves as

\[
\mu(a) \approx \frac{1}{4\pi \eta} \ln \left( \frac{2}{\kappa a} \right) - \gamma,
\]

where \( \gamma = 0.5772 \cdots \) is Euler’s constant. Here the mobility is only weakly (logarithmically) dependent on the disk size \( a \), which is characteristic for 2D fluids. For \( \kappa a \gg 1 \), on the other hand, we have

\[
\mu(a) \approx \frac{1}{\pi \eta (\kappa a)^2},
\]

which shows a stronger algebraic size dependence when compared with the Stokes law for 3D fluids. Such a size dependence can be understood in terms of mass conservation principle because 2D momentum is not conserved any more in the quasi-2D hydrodynamics [26].

Next we explain the hydrodynamic interaction between the two disks immersed in the membrane by using the velocity Green’s function \( G_{\alpha \beta}(\mathbf{r}) \). This tensor gives the flow velocity \( \mathbf{v}(\mathbf{r}) \) of the membrane at \( \mathbf{r} \) due to a point force \( \mathbf{F} \) exerted on the membrane at the origin in the \( xy \)-plane, according to \( v_{\alpha}(\mathbf{r}) = G_{\alpha \beta}(\mathbf{r}) F_{\beta} \) with \( \alpha, \beta = x, y \). The velocity Green’s function can generally be expressed as \( G_{\alpha \beta}(\mathbf{r}) = C_1(r) \delta_{\alpha \beta} + C_2(r)(r_{\alpha}r_{\beta}/r^2) \) where \( \delta_{\alpha \beta} \) is the Kronecker delta and \( r = |\mathbf{r}| \). The longitudinal coupling

\[ \nabla \cdot \mathbf{v} = 0. \]
mobility between the two disks in the membrane can be obtained from \( M(r) = C_1(r) + C_2(r) \), where \( r \) here denotes the distance between the two disks and should satisfy the condition \( r \gg a \). Hence \( M \) does not depend on \( a \) up to the lowest order contribution.

Using the quasi-2D hydrodynamic equations, the longitudinal coupling mobility \( M \) is given by \([27,31]\)

\[
M(r) = \frac{1}{2\pi \eta} \left[ \frac{1}{(kr)^2} - \frac{K_1(kr)}{kr} \right]. \tag{6}
\]

For \( kr \ll 1 \), the above coupling mobility asymptotically behaves as

\[
M(r) \approx \frac{1}{4\pi \eta} \ln \left( \frac{2}{kr} \right) - \gamma + \frac{1}{2}. \tag{7}
\]

For \( kr \gg 1 \), on the other hand, we have

\[
M(r) \approx \frac{1}{2\pi \eta (kr)^2}. \tag{8}
\]

Equations \(7\) and \(8\) are analogous to Eqs. \(4\) and \(5\), respectively, and the physical origins are exactly the same as those for the disk mobility \( \mu \).

### III. THREE-DISK MICROSWIMMER

Having explained the quasi-2D hydrodynamic model for a supported membrane and the resulting mobilities for inclusions, we now investigate the locomotion of a microswimmer in a membrane. To calculate the swimming velocity, we follow the procedure in Ref. \[13\] for a three-sphere swimmer in a 3D bulk fluid. As shown in Fig. 1, we consider a 2D micromachine consisting of three rigid disks of radii \( a_i \) (\( i = 1, 2, 3 \)) that are connected by two arms of variable lengths \( L_j \) (\( j = 1, 2 \)). Such a three-disk microswimmer is immersed in an infinitely large and flat supported membrane having 2D viscosity \( \eta \) and the friction coefficient \( \lambda \), as described before. Each disk exerts a force \( F_i \) on the quasi-2D fluid that we assume to be along the swimmer axis. Without loss of generality, the microswimmer is assumed to move along the \( x \)-axis. In the limit \( a_i/L_j \ll 1 \), we can use Eqs. \(3\) and \(9\) to relate the forces \( F_i \) and the velocities \( V_i \) as

\[
V_1 = \mu(a_1)F_1 + M(L_1)F_2 + M(L_1 + L_2)F_3, \tag{9}
\]

\[
V_2 = M(L_1)F_1 + \mu(a_2)F_2 + M(L_2)F_3, \tag{10}
\]

\[
V_3 = M(L_1 + L_2)F_1 + M(L_2)F_2 + \mu(a_3)F_3. \tag{11}
\]

The swimming velocity of the whole object is obtained by averaging the velocities of the three disks, i.e., \( V = (V_1 + V_2 + V_3)/3 \). Since we are interested in the autonomous net locomotion of the swimmer, there are no external forces acting on the disks. This leads to the following force-free condition:

\[
F_1 + F_2 + F_3 = 0. \tag{12}
\]

As assumed in Ref. \[13\], the motion of the arms connecting the three disks is prescribed by the two given functions \( L_j(t) \). In this situation, the arm motions are related to the velocities as

\[
\dot{L}_1 = V_2 - V_1, \quad \dot{L}_2 = V_3 - V_2, \tag{13}
\]

where the dot indicates the time derivative. The set of six equations in Eqs. \(9\), \(10\), \(11\), \(12\), and \(13\) is sufficient to solve for the six unknown quantities \( V_i \) and \( F_i \) (\( i = 1, 2, 3 \)).

We further assume that arm deformations are relatively small as given by

\[
L_1(t) = \ell_1 + u_1(t), \quad L_2(t) = \ell_2 + u_2(t), \tag{14}
\]

where \( \ell_j \) are constants and \( u_1/\ell_1 \ll 1 \). With these prescribed arm motions, we perform an expansion of the swimming velocity to the leading order in both \( a_i/\ell_j \) and \( u_j/\ell_j \). After some calculations, we finally obtain the average swimming velocity as \[13\]

\[
\bar{V} = G(\langle u_1 u_2 \rangle - \dot{u}_1 u_2), \tag{15}
\]

where \( G \) is the geometric factor to be presented later in Eq. \[18\], and the averaging \( \langle \cdots \rangle \) should be performed by time integration in a full cycle. In the above calculation, the terms proportional to \( u_1 \dot{u}_1, u_2 \dot{u}_2, \) and \( u_1 \dot{u}_2 + \dot{u}_1 u_2 \) are omitted because they average out to zero in a cycle.

As studied for a three-sphere swimmer \[13\], one can assume, for example, that the two arms undergo the following periodic motions:

\[
u_1(t) = d_1 \cos(\Omega t), \quad u_2(t) = d_2 \cos(\Omega t - \phi). \tag{16}\]

Here, \( d_1 \) and \( d_2 \) are the amplitudes of the oscillatory motions, \( \Omega \) is a common arm frequency, and \( \phi \) is a mismatch in phases between the two arms. Then the average swimming velocity in Eq. \[15\] further reads

\[
\bar{V} = G\frac{d_1}{2}d_2 \Omega \sin \phi, \tag{17}
\]

which is maximized when \( \phi = \pi/2 \). When the disks are connected by elastic springs with time-dependent natural lengths, a more general expression for \( \bar{V} \) can be obtained \[17\].

### IV. GEOMETRIC FACTOR

The geometric factor \( G \) (having the dimension of inverse length) in Eq. \[15\] or Eq. \[17\] for a three-disk swimmer in a quasi-2D fluid turns out to be
\[
G(\epsilon, \delta) = \frac{\epsilon_1 \epsilon_2 \epsilon_3 K_0(\epsilon_1) K_0(\epsilon_2) K_0(\epsilon_3) [\epsilon_1 K_0(\epsilon_1) + 4K_1(\epsilon_1)][\epsilon_2 K_0(\epsilon_2) + 4K_1(\epsilon_2)][\epsilon_3 K_0(\epsilon_3) + 4K_1(\epsilon_3)]}{[4\epsilon_1 K_1(\epsilon_1) K_0(\epsilon_2) K_0(\epsilon_3) + 4\epsilon_2 K_0(\epsilon_1) K_1(\epsilon_2) K_0(\epsilon_3) + 4\epsilon_3 K_0(\epsilon_1) K_0(\epsilon_2) K_1(\epsilon_3) + (\epsilon_1^2 + \epsilon_2^2 + \epsilon_3^2) K_0(\epsilon_1) K_0(\epsilon_2) K_0(\epsilon_3)]^2} \\
\quad \times \left[ 2 \left( \frac{1}{\delta_1^3} + \frac{1}{\delta_2^3} - \frac{1}{(\delta_1 + \delta_2)^3} \right) - \left( \frac{K_2(\delta_1)}{\delta_1} + \frac{K_2(\delta_2)}{\delta_2} - \frac{K_2(\delta_1 + \delta_2)}{\delta_1 + \delta_2} \right) \right],
\]

(18)

where \( \epsilon_i = \kappa a_i \) and \( \delta_j = \kappa \ell_j \), and \( K_2 \) is modified Bessel function of the second kind, order two. We note that Eq. (18) is invariant under the exchange of not only the three disks \( a_i \), but also under the exchange of the two arms \( \ell_j \).

For the fully symmetric case with \( a_1 = a_2 = a_3 = a \) and \( \ell_1 = \ell_2 = \ell \), the geometric factor in Eq. (18) reduces to

\[
G(\epsilon, \delta) = \frac{1}{36} \left[ \epsilon^2 + \frac{4\epsilon K_1(\epsilon)}{K_0(\epsilon)} \right] \times \left[ \frac{15}{\delta^3} - \frac{8K_2(\delta)}{\delta} + \frac{2K_2(2\delta)}{\delta} \right],
\]

(19)

where \( \epsilon = \kappa a \) and \( \delta = \kappa \ell \). Equations (18) and (19) are the main results of this paper. In Fig. 2, we plot \( G/\kappa \) as a function of \( \delta \) while keeping the ratio to \( a/\ell = 10^{-2} \). In fact, Eq. (19) has three asymptotic expressions

\[
G(\epsilon, \delta) = \frac{1}{36 \delta [\ln(2/\epsilon) - \gamma]} \quad \text{for } \epsilon \ll 1 \text{ and } \delta \ll 1,
\]

(20)

\[
G(\epsilon, \delta) = \frac{5}{36 \delta^3 \ln(2/\epsilon) - \gamma} \quad \text{for } \epsilon \ll 1 \text{ and } \delta \gg 1,
\]

(21)

\[
G(\epsilon, \delta) \approx \frac{5\epsilon^2}{12\delta^3} \quad \text{for } \epsilon \gg 1 \text{ and } \delta \gg 1.
\]

(22)

FIG. 2. Plot of the scaled geometric factor \( G/\kappa \) [see Eq. (19)] for a fully symmetric 2D microswimmer as a function of the scaled arm length \( \delta = \kappa \ell \) when the disk-to-arm ratio is \( a/\ell = 10^{-2} \). The three asymptotic expressions in Eqs. (20), (21), and (22) are plotted by the dashed lines.

related to the mobility coefficient \( \mu \) and the longitudinal coupling mobility \( M \) by

\[
G(a, \ell) \sim \frac{M(\ell)}{\mu(a)\ell}.
\]

(23)

This relation holds irrespective of the dimensionality of the micromachine and the surrounding fluid \( \kappa^{-1} \). Due to the presence of the hydrodynamic screening length \( \kappa^{-1} \) in a supported membrane, both \( \mu \) and \( M \) exhibit different asymptotic behaviors as shown in Eqs. (4), (5) and Eqs. (7), (8), respectively. Various limiting expressions of \( G \) in Eqs. (20)–(22) can be understood as different combinations of the asymptotic forms of \( \mu \) and \( M \). For example, Eq. (22) showing the scaling \( G \sim (a^2/\ell^2)/\ell \) is a direct consequence of Eqs. (4a) and (8). We also note that, because of the explicit \( 1/\ell \)-dependence in Eq. (23), the logarithmic dependence of \( M(\ell) \) on \( \ell \), as in Eq. (7), does not show up in Eq. (20) within the lowest order expansion.

In order to compare our result with that of a three-sphere swimmer in a 3D fluid, we show here its corre-
sponding geometric factor as obtained in Ref. [13]:

\[ G_{3D} = \frac{3a_1a_2a_3}{(a_1 + a_2 + a_3)^2} \left[ \frac{1}{\ell_1^2} + \frac{1}{\ell_2^2} - \frac{1}{(\ell_1 + \ell_2)^2} \right], \]  

(24)

where \( a_i \) here denote the radii of the three spheres (rather than disks). For the symmetric case with \( a_1 = a_2 = a_3 = a \) and \( \ell_1 = \ell_2 = \ell \), the above expression reduces to

\[ G_{3D} = \frac{7a}{12\ell^2}. \]  

(25)

First, we note that Eq. (24) or Eq. (25) does not depend on the 3D fluid viscosity, while Eq. (18) or Eq. (19) is dependent on the membrane viscosity \( \eta \) through the inverse screening length \( \kappa \). Second, the essential size dependence in Eq. (24) is \( G_{3D} \sim (a/\ell)/\ell \) which does not appear in the previous quasi-2D case. On the other hand, such a dependence is in accordance with the scaling relation Eq. (23) and the Stokes law in a 3D fluid without any characteristic length scale. Hence the existence of the characteristic length scale, \( \kappa^{-1} \), for a quasi-2D fluid completely changes the asymptotic size dependencies of the average velocity. This is an important finding of this paper and highlights the essential difference between 2D and 3D microswimmers.

V. ASYMMETRIC MICROSWIMMERS

Since we have obtained the general expression of the geometric factor \( G \) for a three-disk microswimmer, as shown in Eq. (18), we discuss now the effects of structural asymmetry of a microswimmer on its geometric factor. We first set as \( \ell_1 = \ell_2 = \ell \) and vary the two ratios between the disk sizes as defined by

\[ \Gamma_1 = \frac{a_1}{a_2}, \quad \Gamma_3 = \frac{a_3}{a_2}, \]  

(26)

whereas we keep, for instance, the sum of the three radii being fixed to \( a_1 + a_2 + a_3 = 3a \). In Fig. 4 we plot the scaled geometric factor \( G/\kappa \) in Eq. (18) as a function of the two ratios \( \Gamma_1 \) and \( \Gamma_3 \) when \( \kappa a = 0.1 \) and \( \kappa \ell = 10 \). Notice that \( a/\ell \) should be small within our expansion scheme and the color scale indicates the quantity \( \log(G/\kappa) \). From this plot, we find that the maximum of the geometric factor is realized when the disk size is identical, i.e., \( \Gamma_1 = \Gamma_3 = 1 \). In other words, any asymmetry in the disk size leads to a reduction of the average swimming velocity.

In Fig. 4 we further consider the case when \( \Gamma_1 = \Gamma_3 = \Gamma \) (or, equivalently, \( a_1 = a_3 \)), and plot \( G/\kappa \) as a function of \( \Gamma \). Such a plot corresponds to a cross-section of Fig. 3 along the diagonal line. To compare the quasi-2D case with the 3D case, we also plot \( G_{3D}/\kappa \) [see Eq. (24)] as a function of \( \Gamma \) under the same condition. For \( G_{3D} \), the ratios \( \Gamma_1 \) and \( \Gamma_3 \) correspond to those between the sphere radii. It should be also noted that Eq. (24) does not contain \( \kappa \) and it is used only to compare with the quasi-2D case. Although both \( G \) and \( G_{3D} \) are maximized at \( \Gamma = 1 \), the dependence on \( \Gamma \) is much weaker for \( G \). This weak dependence originates from the logarithmic dependence of the disk mobility \( \mu \) on the disk size \( a \), as shown in Eq. 4.

Alternatively, one can set as \( a_1 = a_2 = a_3 = a \) and
exhibits an algebraic dependence on the distance minimized when the average arm lengths are identical. maximized when the disks are equal-sized, whereas it is microswimmer, and found that the geometric factor is also looked at the effects of structural asymmetry of a toctic behaviors depending on the microswimmer size and the screening length. Our result has been confirmed by screening length in the quasi-2D fluid, membrane. In particular, we have obtained the average disk micromachine swimming in a quasi-2D supported G/κ, G_{3D}/κ vs. Λ

FIG. 5. Plot of the scaled geometric factor G/κ (solid line) [see Eq. (15)] and G_{3D}/κ (dashed line) [see Eq. (22)] as a function of the asymmetry parameter Λ = ℓ_1/ℓ_2 [see Eq. (24)] when κa = 0.1 and κℓ = 10. Notice that a = a_1 = a_2 = a_3 and ℓ = (ℓ_1 + ℓ_2)/2. The minima of G and G_{3D} occur at Λ = 1.

vary the ratio between the arm lengths defined by

Λ = ℓ_1/ℓ_2, \hspace{1cm} (27)

whereas we keep the sum of the two arm lengths being fixed to ℓ_1 + ℓ_2 = 2ℓ. In Fig. 5 we plot the scaled geometric factors G/κ and G_{3D}/κ as a function of Λ when κa = 0.1 and κℓ = 10 as before. Here it is remarkable that both G and G_{3D} are minimized when Λ = 1. On the other hand, the overall behaviors of G and G_{3D} are rather similar because the chosen parameter value satisfies the condition κℓ \gg 1 for which the coupling mobility M exhibits an algebraic dependence on the distance ℓ, as shown in Eq. (5).

VI. SUMMARY AND DISCUSSION

In summary, we have proposed a model of 2D three-disk micromachine swimming in a quasi-2D supported membrane. In particular, we have obtained the average swimming velocity as a function of the disk size and the arm length. Due to the presence of the hydrodynamic screening length in the quasi-2D fluid, κ^{-1}, the geometric factor in the average velocity exhibits various asymptotic behaviors depending on the microswimmer size and the screening length. Our result has been confirmed by the scaling argument for the geometric factor. We have also looked at the effects of structural asymmetry of a microswimmer, and found that the geometric factor is maximized when the disks are equal-sized, whereas it is minimized when the average arm lengths are identical.

At this point, a rough estimate of the characteristic length scales would be useful [23, 29, 31]. The membrane viscosity of lipid bilayers at physiological temperatures is approximately \( \eta \approx 10^{-9} \text{ Ns/m} \) and the viscosity of surrounding water is \( \eta_s \approx 10^{-3} \text{ Ns/m}^2 \). For supported membranes, we can approximate the height of the intervening solvent region as \( h \approx 10^{-9} \text{ m} \). Hence we obtain \( \kappa^{-1} = \sqrt{\eta h/\eta_s} \approx 3 \times 10^{-8} \text{ m} \). We note that this length scale is relatively small and the large scale behavior is expected for micron-sized swimmers.

In our model of a three-disk microswimmer, we have assumed that the three disks are connected by two arms and their time-dependent motions are given by Eq. (14) \[12, 13\]. Alternatively, one can also consider a three-disk microswimmer in which the disks are connected by two elastic springs, while the natural length of each spring is assumed to undergo a prescribed cyclic change. Using the results in Ref. [17], one can immediately estimate the average quantity \( \langle u_1 u_2 - u_1 u_2 \rangle \) in Eq. (14) \[15\] and obtain the average velocity \( \overline{V} \) of an elastic 2D microswimmer. It can be generally shown that the swimming velocity increases with frequency in the low-frequency region, whereas in the high-frequency region, the average velocity decreases when the frequency is increased [17]. Such a behavior originates from the intrinsic spring relaxation dynamics of an elastic swimmer.

Although we have taken into account the hydrodynamic friction between the fluid membrane and the substrate through the friction coefficient \( \lambda \) in Eq. (1), the effect of intrinsic drag of the disks on the substrate was not considered in Eq. (5). One can naturally assume that the drag coefficient of a disk on the substrate is proportional to its area and is given by \( \lambda_d \pi a^2 \), where \( \lambda_d \) is the disk friction coefficient. In this case, the translational mobility coefficient in Eq. (9) will be modified [24]:

\[ \mu(a) = \frac{1}{4\pi\eta} \left[ \frac{(\kappa a)^2}{4} \left( 1 + \frac{\lambda_d}{\lambda} \right) + \frac{\kappa a K_1(\kappa a)}{K_0(\kappa a)} \right]^{-1}. \]  \hspace{1cm} (28)

Notice that the correction term due to \( \lambda_d/\lambda \) gives rise to a contribution that is independent of \( \lambda \). Since only the coefficient of \( (\kappa a)^2 \) is altered when compared with Eq. (22), the drag acting on the disks modifies our result only up to a numerical factor when \( \kappa a \gg 1 \). This means that the asymptotic scaling behaviors in Sec. IV are not affected by the drag forces on the disks. In principle, the disk friction coefficient can be different for different disks. Such an effect can be effectively taken into account by considering different disk radii as long as they are much larger than the screening length \( \kappa^{-1} \).

In this paper, we have discussed the behavior of a 2D microswimmer in a quasi-2D fluid that is characterized by a hydrodynamic screening length, \( \kappa^{-1} \). It should be noted, however, that we encounter a similar situation in which a 3D micromachine swims in a structured viscoelastic fluid having a characteristic length scale. According to our preliminary result, we find that the frequency dependence of the average velocity exhibits fairly
complex behaviors depending on the machine size relative to the characteristic length scale of the surrounding structured fluid. Details of such an investigation will be reported elsewhere [32].

In the future, we shall also investigate the case when the surrounding bulk fluid is viscoelastic [30]. Such a study will enable us to obtain the frequency dependent complex viscosity of the surrounding 3D fluid by measuring the velocity of a 2D microswimmer in a membrane [33]. Such a method will provide us with a new type of non-contact surface microrheology.

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