SN 2014C: VLBI image shows a shell structure and decelerated expansion

Michael F. Bietenholz\textsuperscript{1,2}, Norbert Bartel\textsuperscript{1}, Atish Kamble\textsuperscript{3},
Raffaella Margutti\textsuperscript{4,5}, David Jacob Matthews\textsuperscript{4}, and Danny Milisavljevic\textsuperscript{6}

\textsuperscript{1}Department of Physics and Astronomy, York University, Toronto, M3J 1P3, Ontario, Canada
\textsuperscript{2}SARAO/Hartebeesthoek Radio Observatory, PO Box 443, Krugersdorp, 1740, South Africa
\textsuperscript{3}formerly at Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, Cambridge, MA 02138, USA
\textsuperscript{4}Center for Interdisciplinary Exploration and Research in Astrophysics (CIERA) and Department of Physics and Astronomy, Northwestern University, Evanston, IL 60208, USA
\textsuperscript{5}CIFAR Azrieli Global Scholar, Gravity & the Extreme Universe Program, 2019
\textsuperscript{6}Department of Physics and Astronomy, Purdue University, 525 Northwestern Ave., West Lafayette, IN 47907, USA

Accepted for publication in MNRAS

ABSTRACT

We report on new Very Long Baseline Interferometry radio measurements of supernova 2014C in the spiral galaxy NGC 7331, made with the European VLBI Network \textasciitilde 5 yr after the explosion, as well as on flux density measurements made with the Jansky Very Large Array (VLA). SN 2014C was an unusual supernova, initially of Type Ib, but over the course of \textasciitilde 1 yr it developed strong H\textalpha lines, implying the onset of strong interaction with some H-rich circumstellar medium (CSM). The expanding shock-front interacted with a dense shell of circumstellar material during the first year, but has now emerged from the dense shell and is expanding into the lower density CSM beyond. Our new VLBI observations show a relatively clear shell structure and continued expansion with some deceleration, with a suggestion that the deceleration is increasing at the latest times. Our multi-frequency VLA observations show a relatively flat powerlaw spectrum with \( S_{\nu} \propto \nu^{-0.56\pm0.03} \), and show no decline in the radio luminosity since \( t \sim 1 \) yr.

Key words: Supernovae: individual (SN 2014C) – radio continuum: general

1 INTRODUCTION

Supernova (SN) 2014C was a very unusual supernova, and its progenitor had complex mass-loss in the time before the explosion. SN 2014C was discovered on 2014 January 5 in the nearby early-type spiral galaxy NGC 7331 by the Lick Observatory Supernova Search (Kim et al. 2014). We adopt the updated Cepheid distance of \( D = 15.1 \pm 0.7 \) Mpc from Saha et al. (2006)\textsuperscript{1}, and an explosion date, \( t = 0 \), of 2013 December 30.0 (UT) = MJD 56656.0, as determined by Margutti et al. (2017) from bolometric lightcurve modelling.\textsuperscript{2}

At its discovery, SN 2014C had the spectrum of ordinary, H-stripped Type Ib supernova (Kim et al. 2014; Tartaglia et al. 2014). Unfortunately, no spectra could be obtained for several months thereafter as it went behind the sun, but after it emerged, the spectrum had evolved into a Type IIn one, with prominent H\textalpha lines, which implied strong interaction with the circumstellar medium (CSM) (Milisavljevic et al. 2015; Margutti et al. 2017). At \( t = 20 \) d, it was faint in X-rays, but, unusually, rose till \( t \sim 1 \) yr and has remained high since (Margutti et al. 2017; Jin & Kong 2019). In the mid-infrared, it had a high and almost constant brightness till \( t \sim 5.5 \) yr (Tinyanont et al. 2019).

SN 2014C was quickly also detected in the radio, at frequencies ranging from 7 GHz to 85 GHz (Kamble et al. 2014; Zauderer et al. 2014). In the first month, it did not have a high radio luminosity (\( L_{\nu} \sim 10^{26} \text{ erg s}^{-1} \text{ Hz}^{-1} \) at 7 GHz, Kamble et al. 2014). However, the luminosity rose rapidly after about one month, and then again around 1 yr (Anderson et al. 2017), and has stayed high. Due to its relative nearness and high radio brightness it was a target for Very Long Baseline Interferometry (VLBI) observations. In Bietenholz et al. (2018), which we will refer to as Paper I hereafter, we presented our first four epochs of VLBI observations, between \( t = 1.1 \) and 2.9 yr, which showed that SN 2014C’s forward shock was expanding at \( v \sim 13\,600 \) km s\(^{-1}\) over that period, but must have been expanding more rapidly at \( t < 1 \) yr.

The picture of SN 2014C that has emerged (e.g. Milisavljevic et al. 2015; Margutti et al. 2017) is that the supernova exploded as a Type Ib, having lost most of its H envelope, inside a low-density cavity. Due to the low density there was

\footnotesize
\textsuperscript{1} The NASA/IPAC Extragalactic Database (NED), \url{https://ned.ipac.caltech.edu}, lists 54 redshift-independent distances, with mean and standard deviation 13.4 \pm 2.7 Mpc.
\textsuperscript{2} Although SN 2014C’s explosion date is not tightly constrained, it is uncertain by less than one week, and the exact value will have little effect on our results which are at times several years after the explosion.

\textcopyright 2021 The Authors
relatively little radio or X-ray emission initially. As the shock moved outward, at \( t \sim 0.3 \) yr it encountered a shell of very dense circumstellar material (CSM), causing emission at both X-rays and radio to brighten. Interaction with the CSM commonly produces both radio and X-ray emission (e.g. Chevalier & Fransson 2017).

The shell was formed due to a mass ejection event shortly before the SN explosion. The shock has since progressed through this overdense shell, and is currently expanding through the moderately dense wind of the progenitor from the time before the ejection event.

In the few cases, like SN 2014C, where a SN is near enough to be resolved with VLBI observations, they can provide crucial direct observational constraints on basic physical parameters of the SN, in particular the (time-dependent) radius of the expanding ejecta and the corresponding expansion speed. In Paper I, we used VLBI observations to determine the radius, \( r \), of the shock in SN 2014C at various epochs, and found a radius of \( r_{16} = 14.4 \pm 0.6 \), at \( t = 2.9 \) yr, where \( r_{16} \) is a dimensionless radius, and is equal to \( r/(10^{16} \text{ cm}) \).

In order to continue to study the evolution of SN 2014C, we made new VLBI observations, this time with the European VLBI Network (EVN), \( \sim 2 \) yr after those presented in Paper I. Our new image has the highest resolution relative to the shell size for this SN to date. We also report on observations with the Karl G. Jansky Very Large Array of the National Radio Astronomy Observatory (NRAO) in the U.S.A. to measure the total flux density and spectral energy distribution (SED) in early 2020.

2 OBSERVATIONS AND DATA REDUCTION

2.1 VLBI Observations

We observed SN 2014C using the EVN on 2018 October 30 and 31 at 8.4 GHz (observing codes EB066A, EB066B). Both observations used a standard 1-Gbps experiment setup (8 sub-bands, 16 MHz bandwidth per sub-band, dual circular polarisation, 2-bit quantisation). The participating telescopes were Westerbork (Wb, phased-array), Effelsberg (Et), Medicina (Mc), Onsala (Os), Tjanna (T6), Urumqi (Ur), Yebes (Ys), Hartebeesthoek (Hh) Svetloe (Sv), Zelenchukskaya (Zc), Badary (Bd) and Irbene (Ir). The correlation was done by the EVN software correlator (SFXC; Keimpema et al. 2015) at JIVE (Joint Institute for VLBI, ERIC) using standard correlation parameters of continuum experiments. Each of the two runs was 8 h in length.

We phase-referenced our observations to the source VCS1 J2248+3718, which we will refer to as just J2248+3718, and which is 2.9° away from SN 2014C on the sky. We found it to be only marginally resolved\(^3\). We show the image of J2248+3718 in Figure 1. Our phase-referencing calibration for SN 2014C, which provided the starting point for the phase self-calibration of SN 2014C, was based on the CLEAN model of J2248+3718.

The data reduction was carried out with NRAO’s Astronomical Image Processing System (AIPS). The initial flux density calibration was done through measurements of the system temperature at each telescope, and improved through self-calibration of the phase-reference sources. The signal-to-noise ratio on SN 2014C was high enough to permit self-calibration in phase. We started with self-calibrating the antennas T6, Bd, and Ir, which showed the most obvious failures in phase-referencing and exhibited phase-wrapping, due in part to inaccurate antenna positions. We used a 15 min solution interval, and an initial CLEAN model made excluding the data from those three antennas. We then proceeded to include those three antennas in the imaging and the other antennas in the self-calibration, with a longer solution interval of 2 h, but overlapped so that we obtained a solution every hour. Both imaging and model-fitting results for SN 2014C are derived from the phase self-calibrated data.

2.2 VLA Observations

We observed SN 2014C also with the VLA on 2020 May 6, (observing code 20A-441). The total length of the observing run was 2 h, and we observed at frequencies between 2 and 20 GHz. The data were reduced following standard procedures using the Common Astronomy Software Application (CASA; McMullin et al. 2007), with the flux density scale set by observations of 3C 286. The SN 2014C data were self-calibrated in phase only.

We measured flux densities by fitting an elliptical Gaussian of the same dimension as the CLEAN beam to the image, with a zero-level also being fit in cases where there was significant background emission from the galaxy, although in all cases the galaxy background was less than the uncertainties. Our uncertainties include the statistical contribution due to the noise in the images, but are dominated by the 5% uncertainty in the flux-density calibration at the VLA.

\(^3\) In Paper I we had used the nearer NVSS J223555+341837 as a phase-reference source, but we found it to be significantly resolved, and we therefore switched to the less-resolved J2248+3718 for these observations. Since we were able to phase self-calibrate SN 2014C at 8.4 GHz both in this work and in Paper I, any structure in reference sources should not affect our results.
3 RESULTS
3.1 VLBI image

We show the VLBI image of SN 2014C, obtained on 2018 Oct. 31, or $t = 4.8$ yr, in Figure 2. The image was deconvolved using the CLEAN algorithm, with AIPS robustness parameter set to $+0.5$. To increase the reliability of the images we used the square root of the data weights in the imaging, which results in more robust images less dominated by a small number of very sensitive baselines. We also use the multi-scale extension of the original CLEAN algorithm, MS-CLEAN (Wakker & Schwarz 1988), which produces superior results for extended sources (see, e.g., Hunter et al. 2012; Rich et al. 2008; Bietenholz et al. 2010b). The total CLEANed flux density was 15.8 mJy, the rms background brightness was 51 $\mu$Jy beam$^{-1}$, and the FWHM resolution was $1.17 \times 0.54$ mas at p.a. 5$^\circ$.

The image shows a structure that is at least approximately circular in outline, with enhancement to the east and west, with the one in the east being about 25% brighter. An east-west asymmetry of similar magnitude was seen in our image from $t = 2.9$ yr in Paper I, but in the opposite sense, with the west side being brighter. Such one-sided asymmetries in the radio brightness seem to be common in SNe (Bietenholz 1993J, Bietenholz et al. 2003), but their origin is not known.

Is the enhancement in brightness to the east and west real, or is it merely due to the convolution of a circular ring-like brightness pattern with a north-south elongated restoring beam? To answer this question, we simulated visibility measurements for a source with complete circular symmetry, which simulated visibilities had the same elongated $u$-$v$ coverage, and thus the same elongated restoring beam as our EVN observations. We added random Gaussian noise to the simulated visibilities, scaled so as to produce the same image background rms as was found in the image made from the real data. We then deconvolved these simulated visibilities in the same fashion as the real data. Our source model was the projection of a spherical shell of emission, with a ratio of outer to inner radius, $R_{o/i} = 1.1$ (we justify this choice in Section 3.2 below). We show the resulting simulated image in Figure 3. The image looks very similar to the real VLBI image in Figure 2, in particular in also having enhanced brightness to the E and W.

While the real image has brightness contrasts of $\sim 2.2:1$ between the hot spots to the east and west and the corresponding “gaps” to the north and south, the simulated one with $R_{o/i} = 1.1$ had brightness contrasts of 1.4:1, which would increase if smaller values of $R_{o/i}$ were used for the model. This suggests that a significant part of the brightness enhancement to the east and west in our image is due merely to our elongated beam, although there may also be some real enhancement particularly to the east, where the observed image has higher brightness.

Our simulated data differ from the real measurements in one respect. Although we scaled the noise added to the simulated visibilities to produce the same image background rms, the noise we added was uncorrelated between visibilities. The real visibilities, on the other hand, are corrupted both by random and uncorrelated noise and by residual calibration errors. Since the calibration is antenna-based, this introduces correlations in the visibility errors for the real data not present in the simulated data. Since we phase self-calibrated the residual calibration errors should be small, and it seems unlikely that such correlated errors would cause systematic changes in the apparent image morphology.
3.2 Size and Expansion Speed

To determine a precise size for SN 2014C, we fit a geometrical, spherical-shell model in the Fourier transform or $u$-$v$ plane, as we did in Paper I\(^4\).

We used the same model we used in Paper I, which is the Fourier transform of the projection of an optically thin shell of emission. The model is characterized by the inner and outer angular radii of the shell, $\theta_i$, $\theta_o$, and the total flux density. We again used the square root of the data weights in the fitting, which makes the results more robust at the expense of some statistical efficiency.

We justify this choice of model geometry for SN 2014C in Paper I, and the same geometry has been found appropriate for other SNe (e.g. Bartel et al. 2002; de Witt et al. 2016). It is the outer angular radius, $\theta_o$, which is most closely identified with the forward shock, and which is also most reliably determined by the data. We therefore first fix the ratio of $\frac{\theta}{\theta_o}$ simulations (Jun & Norman 1996). The fitted value of $\theta_o$ is the outer angular radius, for other SNe (e.g. Bartel et al. 2002; de Witt et al. 2016). It includes three contributions in our final standard error, added in quadrature.

The first contribution was estimated using jackknife resampling (McIntosh 2016). Specifically, we dropped the data from each of the antennas in the VLBI array in turn and calculated $N_{\text{antenna}} = 12$ new estimates of the fitted size, and the scatter over these 12 values allows one to estimate the uncertainty in the outer angular radius $\theta_o$. We follow the same procedure as in Paper I to estimate a systematic uncertainty, and again include three contributions in our final standard error, added in quadrature.

We then take our final value for $\theta_o$ to be the midpoint of the two values obtained for $R_{o/i}$ fixed at 1.25, and $R_{o/i}$ free (with the fitted value $R_{o/i} = 1$), and add in quadrature half the difference in those two values of $\theta_o$ to the uncertainty we had determined in the fixed $R_{o/i} = 1.25$ case, to obtain a final value for $\theta_o$ of $0.89 \pm 0.08$ mas. At the distance of SN 2014C (15.1 Mpc), this radius corresponds to a linear size of $r_{16} = 20.1 \pm 1.7$.

3.3 Expansion Curve

We plot our new value for the radius at $t = 4.8$ yr along with earlier ones from Paper I, in Figure 4. The expansion of SNe is often parameterized as a powerlaw, such that $r = r_{1\text{yr}}(t/\text{yr})^m$, where $r$ is the radius of the supernova at time $t$, $r_{1\text{yr}}$ is the radius at $t = 1$ yr, and $m$ is the powerlaw coefficient, often called the expansion parameter. Such a function has been shown to be expected on theoretical grounds with $m$ in the range 0.6 to 1 (e.g. Chevalier 1982b), and used to describe other SNe (e.g. SN 1993J Bartel et al. 2002).

The velocity between our previous measurement of $r$ at $t = 2.9$ yr (Paper I) and the present one at $t = 4.8$ yr is $9400 \pm 2900$ km s$^{-1}$. If we interpret the evolution as a powerlaw, the values at $t = 2.9$ and 4.8 yr imply $m = 0.66 \pm 0.18$, suggesting that, compared to the average velocity since the explosion, there is a moderate amount of deceleration over the last two measurements.

We turn now to fitting all the radius measurements. We fit the same two functions we used in Paper I to our measurements of $r_{16}$ by least squares, and we refer the reader to that paper for a fuller discussion of the choice of functions. The first function is the powerlaw function just described.

Fitting a powerlaw function to our radius measurements, we obtain:

$$r_{16} = (6.27 \pm 0.22) \cdot \left(\frac{t}{1\text{yr}}\right)^{0.77 \pm 0.03} \left(\frac{D}{15.1\text{Mpc}}\right),$$

with a sum of squared residuals, SSR = 2.4. We plot this fitted expansion curve as the red line in Figure 4. The fitted value $m$ is higher, albeit not significantly so, than that of $m = 0.66 \pm 0.18$ obtained from only the last two measurements, suggesting a possible increase in deceleration at the latest times.

\(^4\) Bietenholz et al. (2010a) showed that in the case of SN 1993J, the results obtained through $u$-$v$ plane modelfitting are superior to those obtained in the image plane.
The fitted expansion curve, with $m = 0.77$, suggests a moderate amount of deceleration over the history of the SN. This value of $m$ is consistent with what is generally expected from the mini-shell model. If the CSM has a wind density profile ($\rho \propto r^{-3}$), then the mini-shell solution has that $m = (n - 3)/(n - 2)$ (Chevalier 1982b), so our value of $m$ suggests ejecta with $\rho \propto r^{-n}$ with a relatively flat value of $n = 6.5^{+0.6}_{-0.5}$.

In the self-similar solution of Chevalier (1982a), the value of $R_{o/i}$ depends on $n$, and for $n = 6.5$ a value of $R_{o/i} \approx 1.3$ is expected, whereas our model-fitting suggested smaller values of $R_{o/i} \lesssim 1.25$ (Section 3.2). However, since the density structure of SN 2014C’s CSM was clearly more complex than a simple $\rho \propto r^{-2}$ powerlaw assumed in the self-similar model, we should expect that the relationships between $m$, $n$ and $R_{o/i}$ will deviate somewhat from those in the self-similar case.

There are, however, good reasons to think that a simple powerlaw may not be appropriate to describe SN 2014C’s expansion. As we described in the introduction, at about $t \sim 0.3$ yr, SN 2014C’s expanding shock seems to have encountered a region of dense, H-rich CSM, leading to an evolution that deviates from the self-similar powerlaw function of the mini-shell model. Systems of this nature have been considered by numerous authors (Chevalier & Liang 1989; Chugai & Chevalier 2006; Smith & McCray 2007; van Marle et al. 2010). In such a system, the shock slows dramatically when it first encounters the dense shell. It then accelerates as it emerges from the dense CSM shell, and subsequently coasts to coast at almost constant speed until the mass of the CSM swept up from outside the massive shell becomes comparable to the shell mass, at which point an approximately power-law expansion resumes. This behaviour has been reproduced in numerical simulations by van Marle et al. (2010).

The impact of the SN shock on the dense CSM shell for SN 2014C occurred at $t \sim 0.3$ yr, before the first VLBI observations at $t = 1.1$ yr. We cannot, therefore, directly resolve the slowing of the shock, so we model only the period of approximately constant-velocity expansion after the impact of the shock on the massive shell. Hence, the second function that we fit to SN 2014C’s expansion, which we call the “constant velocity” function, is $r[t > t_{\text{impact}}] = r_{\text{impact}} + v_{\text{post}} \cdot (t - t_{\text{impact}})$, where $t_{\text{impact}}$ is the time at which the shock impacts on the dense shell, $r_{\text{impact}}$ is the radius at that time, and $v_{\text{post}}$ is the shock velocity after that time. For $t_{\text{impact}} \leq 1$ yr, that function is equal to $r = r_{\text{yr}} + v_{\text{post}} \cdot (t - 1)$, so we fit the latter function and avoid the problem of not knowing $t_{\text{impact}}$ exactly. It is expected that $t_{\text{impact}}$ is in the range $0.3 \sim 0.6$ yr (e.g. Harris & Nugent 2020). We again fit the function to the VLBI radius measurements using weighted least squares.

Note that the powerlaw function also produces constant-velocity expansion when $m = 1$, but there is a crucial difference between the two functions: the powerlaw function with $m = 1$ is just uninterrupted free expansion starting from $r = 0$, $t = 0$, whereas our constant velocity function only has a constant velocity after $t = 1$ yr, and does not extrapolate to $r = 0$, $t = 0$, since a more rapid expansion at $t < 1$ yr is implicit.

Fitting the constant-velocity function, we obtained

$$r_{16} = (6.27 \pm 0.22) + (4.12 \pm 0.22) \times \left(\frac{t}{1 \text{ yr}} - 1\right) \left(\frac{D}{15.1 \text{ Mpc}}\right),$$

where the fitted radius at 1 year is $(6.27 \pm 0.22) \times 10^{16}$ cm and the post-impact velocity is $v_{\text{post}} = (4.12 \pm 0.22) \times 10^{16}$ cm yr$^{-1}$, or $13040 \pm 690$ km s$^{-1}$. The SSR of this fit was 3.7, and we plot the fitted function as the blue line in Figure 4.

The SSR values for the powerlaw and the constant velocity fitted functions were 2.4 and 3.7 respectively, and therefore our data do not distinguish reliably between the two, although the powerlaw function is a slightly better fit. The values of SSR are close to the most probable value for a Chi-squared distribution with 5 degrees of freedom, $\chi^2 = 3$, indicating a reasonable fit, although we note that our measurement errors are likely correlated, so the SSR is likely not exactly $\chi^2$-distributed. The slightly better fit of the powerlaw form may be due to the constant-velocity period having ended and the powerlaw expansion resuming, as is expected at late times after the impact of the ejecta on the CSM shell (Harris & Nugent 2020).

### 3.4 VLA Flux Density Measurements

On 2020 May 6, we measured the flux density of SN 2014C over a range of frequencies between 3.0 and 23 GHz. We show the SED in Figure 5. A powerlaw with spectral index, $\alpha = -0.56 \pm 0.03$, (where $S_{\nu} \propto \nu^\alpha$), and $S_{\nu=5 \text{ GHz}} = 21.6 \pm 0.6$ mJy fits all the measurements to within the uncertainties, with the SSR (sum of squared residuals) being 2.4, which is close to the expectation value of $\chi^2_3$. 

---

**Figure 4.** The radius of SN 2014C as a function of time, $t$, since the explosion at $t = 0$ on 2013 Dec. 30. The outer radii were determined by fitting a spherical shell model directly to the visibilities in this paper and in Paper I, and calculated for a distance of $D = 15.1$ Mpc. Radii measured at 8.4 GHz are shown as black circles and those at 22 GHz as green squares. We show two different functions fitted to the measured radii. The first, shown by the solid (red) line, is an uninterrupted powerlaw expansion of the form $r \propto t^{n=0.77}$. The second, shown by the dashed (blue) line, is a constant velocity expansion after $t = 1$ yr (with an implied more rapid expansion before then). We expect the approximately constant-velocity regime to begin at $t \sim 1$ yr; hence, we show the extrapolation of the constant velocity fit to earlier times with a dotted line.
Table 1. VLA Flux Density Measurements on 2020 May 6

| Frequency (GHz) | Flux Density (mJy) |
|----------------|--------------------|
| 3.0            | 27.9 ± 1.4         |
| 6.0            | 20.9 ± 1.1         |
| 10.0           | 14.3 ± 0.7         |
| 15.1           | 11.6 ± 0.6         |
| 22.4           | 9.8 ± 0.5          |

* Our standard errors include the image background rms values and a 5% flux-density calibration error, added in quadrature.

We give the flux densities measured from our VLA observations in Table 1. We show the 4.9 GHz and 7.1 GHz lightcurves in Figure 6, where we also show for comparison the 15.7 GHz lightcurve measured by the Arcminute Microkelvin Imager from Anderson et al. (2017). The lightcurves do show the usual pattern of an earlier rise at higher frequencies. However, the overall nature of the lightcurve is quite unusual, with a slow rise till \( t \sim 0.6 \) yr that occurs in steps at least at 15 GHz, followed by a flat curve with an almost value for the almost 6 yr since \( t \sim 1 \) yr.

4 DISCUSSION

4.1 Morphology of SN 2014C

The new VLBI image of SN 2014C at \( t = 4.8 \) yr (Fig. 2) confirms the shell structure suggested by our earlier VLBI image from \( \sim 2 \) yr earlier (Paper I). The source remains relatively circular in outline. Two enhancements in brightness are visible to the east and west. These are likely largely due to convolution of a ring-like pattern with an elliptical restoring beam, rather than being intrinsic brightness enhancements, fortuitously aligned with the restoring beam. In our tests with synthetic data, a completely circularly symmetric shell model produces an image very similar to the observed one when convolved with our elliptical restoring beam (see Section 3.1, Figure 3).

Although a spherical shell structure is consistent with our VLBI image, could SN 2014C in fact have a different structure? Given the observed image (Figure 2), is it possible that the source is intrinsically bipolar or elliptical, rather than having a spherical shell structure? Bi-polar jets occur in GRB and possibly in some SNe (e.g. Papish & Soker 2011). SN 1987A, on the other hand, has a structure that is axially, but not spherically symmetric (e.g. McCray & Fransson 2016).

To compare a possible bipolar structure to the spherical shell structure, whose projection onto the sky-plane is circularly symmetrical, we fitted a model consisting of two circular Gaussians to directly the visibilities in the same way we fitted the spherical shell model in Section 3.2. We found the fit considerably poorer, despite the two-Gaussian-component model having more free parameters. We can therefore say that the observations disfavour a simple bipolar structure.

A circular ring-like structure at some angle to the plane of the sky, similar to SN 1987A’s equatorial ring, is harder to constrain in this manner, and if the ring is oriented near to the plane of the sky the projected image will strongly resemble the projection of a thin spherical shell. A tilted ring structure of this nature could therefore be also compatible with the VLBI image. Future VLBI observations at higher relative resolution may allow us to more definitely determine the emission geometry.
4.2 Radius and Expansion Speed

From our VLBI measurements, we determined the radius of the radio emission region, which probably corresponds to the radius of the forward shock (see Bartel et al. 2007, for a discussion on the relationship between the radio emission region and the forward shock in the case of SN 1993J). At $t = 4.8$ yr, we measured a radius of $r_{16} = 20.5 \pm 1.8$ (for $D = 15.1$ Mpc). The velocity between our previous measurement at $t = 2.9$ yr (Paper I) and the present one is $9400 \pm 2900$ km s$^{-1}$.

This velocity is consistent within the uncertainties, but lower by 0.8s, than the value of $14000 \pm 4200$ km s$^{-1}$ we found between $t = 2.3$ and 2.9 yr (Paper I), suggesting that the shock front is likely decelerating somewhat.

We found in §3.3 that a powerlaw model fits all the VLBI radius measurements marginally better than a constant velocity model (see Fig. 4). Our latest radius measurement ($t = 4.8$ yr) suggests a possible increase in the deceleration at the latest times, in either the constant-velocity or the powerlaw models of the expansion. Further VLBI measurements should be undertaken to better constrain any change in deceleration.

Given the complicated nature of SN 2014C’s CSM, with, going outward, first a low-density cavity, then a very dense shell, then a moderately dense stellar wind, the real expansion curve will be more complex than a simple powerlaw. In Paper I we compared the evolution of SN 2014C to scaled hydrodynamic simulations from van Marle et al. (2010) to show the generally expected behaviour of a SN shock slowing down dramatically upon first encountering a thick shell, but the shock speed then recovering somewhat.

Since then, Harris & Nugent (2020) have performed new hydrodynamic simulations more specifically aimed at cases like SN 2014C. They find the measurements can be accounted for by their flattest value of $\alpha$ for 14 different SNe, and our value for SN 2014C is close to their flattest value of $\alpha = -0.55$ (which was for the Type III SN 1970G).

The relatively flat spectrum of SN 2014C might just be due to a slow transition from optically-thick (invoked spectrum) to optically-thin. As can be seen from the 4.9 and 7.1 GHz lightcurves in Fig 6, the spectrum between these two frequencies remained inverted until $t \sim 3$ yr. If the spectrum were still transitioning between optically thick and thin, one would expect significant curvature in the spectrum, with a steep spectrum at high frequencies and a flat (or inverted one) at low frequencies. Indeed, our lowest-frequency measurement at 3 GHz suggests a marginally flatter spectrum below 6 GHz. If we fit only the points at 6 GHz and above, we obtain $\alpha = -0.61 \pm 0.04$, which is within the normal range.

Bartel et al. (2002) found also that the optically-thin value of $\alpha$ for the Type IIn SN 1993J became flatter with time. Maeda (2013) shows that such a flattening is in fact expected, with the shock acceleration being less efficient in young SNe where the shock speed is high, leading to steeper spectra, and becoming more efficient later on, leading to flatter spectra for supernova remnants, for which $\alpha$ clusters around the expected value for shock acceleration of $\alpha = -0.5$. This process may also be occurring in SN 2014C, and contributing to the relatively flat value of $\alpha$.

4.4 Radio Lightcurve

From our VLA observations at $t = 6.3$ yr we found that the lightcurve has an extended, almost constant, plateau since $t \sim 0.8$ yr. Such a lightcurve is unusual, the lightcurves of the majority of SNe show an approximately powerlaw decline after a time on the order of one month (e.g. Weiler et al. 2002; Bietenholz et al. 2020).

The strong and sustained radio emission is interpreted as being due to the strong CSM interaction as the forward shock ploughed through the dense CSM shell. The rate of particle acceleration is dependent on the CSM density but is also strongly dependent on the shock velocity. Harris & Nugent (2020) show that while the CSM density drops when the shock emerges from the dense shell, the shock speed increases which can lead to an increase in radio emission despite the drop in CSM density.

However, these increases in the shock velocity are temporary, and since the shock emerged from the dense shell some time ago, why is the radio brightness still staying high? In the self-similar mini-shell model of a SN, where both the ejecta and the CSM density structures are powerlaws in radius, the radio brightness evolves as $S \propto t^\beta$ (Fransson et al. 1996), with

$$\beta = -[3 - \alpha - (6 - \alpha - (s/2)(3 - \alpha))/((n-3)/(n-s))]$$

where the density of the CSM is $\propto r^{-s}$, that of the ejecta is $\propto r^{-n}$, and $\alpha$ is the radio spectral index. Although in the case of SN 2014C, it is clear that the CSM structure is more complex than a simple powerlaw, and strictly self-similar evolution is therefore not expected, it is nonetheless instructive to compare SN 2014C’s evolution to expectations from the self-similar case. It is expected that at some point after the shock has passed through the dense CSM, the evolution would once again approach being self-similar. Since the radio brightness of SN 2014C has not declined much, $\beta \approx 0$. For a typical value of $n = 16$ and our observed $\alpha = -0.56$, in a self-similar scenario we would have $s = 1.45$. Since SN 2014C’s evolution was not self-similar, the actual value of $s$ will probably differ.

However, the shock exited the dense CSM shell already at $t \sim 0.3$ yr, so by $t \sim 6.3$ yr probably SN 2014C’s evolution is again approaching the self-similar solution, and that value of $s$ at least approximately correct. The flat lightcurve therefore probably suggests a CSM density profile notably flatter than that for a steady wind ($\propto r^{-2}$). The exact value of
n has only a minor effect on this conclusion, which holds for any reasonable value of n.

Harris & Nugent (2020) suggest that SN 2014C’s shock crossed through a dense shell of CSM, and is now interacting with a wind CSM, with s = 2. While this scenario fits the measured sizes and expansion velocities, it is hard to reconcile with the lack of any decay in the radio luminosity. The flat lightcurve suggests ν ∝ t−0.5, implying that the shock is currently interacting with CSM from a period where the progenitor’s mass-loss was relatively steadily decreasing with time. Harris & Nugent (2020) found that both models with s = 2 (a steady wind) and s = 1 (wind with density decreasing with time) were compatible with the measurements, therefore a model with s = 1.5 should also be compatible with the data.

The decrease in time of the mass-loss rate of the progenitor must have occurred only over a bound period, and there was likely steadier mass-loss rate before the decrease. The shock radius is currently 2.05 × 10^17 cm. If we assume a wind speed of 1000 km s^{-1}, typical of a Wolf-Rayet like progenitors, the shock is currently interacting with material lost from the star only about a century before the explosion. Even if the wind speed was 10 km s^{-1}, typical of supergiants, the age of the material is only of order 10^7 yr. Fluctuations in the mass-loss rate over these timescales, short compared to the age of the star, have been seen or inferred in a number of stars (e.g. Smith 2014). It is likely, therefore, that the lightcurve will turn over and decrease in the future as the shock moves beyond the region formed by the mass-loss that was declining in time prior to the massive shell ejection shortly before the explosion.

5 SUMMARY AND CONCLUSIONS

We report on our new VLBI and VLA observations of SN 2014C. We resolved the radio emission from the expanding shell of ejecta and determined the radius of the emission region at t = 4.8 yr after the explosion. Comparing these results with those of our earlier VLBI measurements, we found the following:

1. Our new VLBI observations show a structure which is relatively circular in outline and enhanced towards the outer edge. There is a clear enhancement to the east and west, much of which is likely not intrinsic, but rather due to the convolution with an elongated restoring beam. Some intrinsic enhancement of the surface brightness does however seem likely, particularly to the east. The observed image is compatible with a relatively thin spherical shell seen in projection. Our model fits show that a simple bipolar structure is unlikely. A ring-like structure, however, could also be compatible with the image.

2. At t = 4.8 yr, the angular outer radius of the supernova was 0.91 ± 0.08 mas, corresponding to (20.5 ± 1.8) × 10^16 cm (for a distance of 15.1 Mpc). The speed between the last two epochs of VLBI observations (t = 2.9 and 4.8 yr) was 9400 ± 2900 km s^{-1}.

3. The expansion of SN 2014C, as determined from VLBI observations (t = 1.1 – 4.8 yr) is compatible with powerlaw expansion, with r ∝ t^{-0.77±0.03}, suggesting a moderate amount of deceleration over the SN’s lifetime. The measurements are compatible with an early deceleration, and an approximately constant-velocity expansion with 13040 ± 690 km s^{-1} since t = 1.1 yr. There is a suggestion that the deceleration is increasing again after t ∼ 3 yr.

4. The radio spectral energy distribution is consistent with a powerlaw with S ∝ ν^{α}, where α = −0.56 ± 0.03. This value of α is somewhat flatter than that seen in the majority of SNe. There is a hint of flattening of the spectrum below 6 GHz, as might be expected if it were just now becoming optically thin at low frequencies.

5. The radio lightcurve at ~6 GHz had reached a peak of ~25 mJy, corresponding to a νL_ν luminosity of 4.1 × 10^{37} erg s^{-1}, after about one year, and has stayed almost constant since then, up to our latest measurement at t = 6.3 yr. Our observations are consistent with a picture that has emerged of SN 2014C having a mass-loss event that ejected a very dense shell not long before the explosion, with the mass-loss rate prior to the shell ejection being much lower.

6. The sustained radio emission since t ∼ 1 yr suggests that the progenitor went through a period of steadily decreasing mass-loss before ejecting the dense shell and then exploding as a SN.

ACKNOWLEDGEMENTS

We thank the teams of both the EVN and the VLA for their work to make the observations possible. The EVN is a joint facility of independent European, African, Asian, and North American radio astronomy institutes. The National Radio Astronomy Observatory is a facility of the National Science Foundation operated under cooperative agreement by Associated Universities, Inc. We have made use of NASA’s Astrophysics Data System Abstract Service. This research was supported by both the National Sciences and Engineering Research Council of Canada and the National Research Foundation of South Africa.

We also thank the anonymous referee for his or her comments which improved the paper.

DATA AVAILABILITY STATEMENT

The raw data underlying this paper are available in EVN and NRAO archives, and can found under the observing codes EB066A, EB066B for the EVN and 20A-441 for NRAO. The calibrated data or images underlying this paper will be shared on reasonable request to the corresponding author.

REFERENCES

Anderson G. E., et al., 2017, MNRAS, 466, 3648
Bartel N., et al., 2002, ApJ, 581, 404
Bartel N., Bietenholz M. F., Rupen M. P., Dwarakadas V. V., 2007, ApJ, 668, 924
Bartel N., Karimi B., Bietenholz M. F., 2017, Astronomy Reports, 61, 299
Bietenholz M., 2014, in Tarchi A., Giroletti M., Feretti L., eds, 12th European VLBI Network Symposium and Users Meeting (2014), published by SISSA, Trieste, p. 51
Bietenholz M. F., Bartel N., 2017, ApJ, 851, 124
Bietenholz M. F., Bartel N., Rupen M. P., 2003, ApJ, 597, 374
