Ellipsoidal Variability and the Difference between Sequence D and E Red Giants

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ABSTRACT

We have studied a sample of Large Magellanic Cloud red giant binaries that lie on sequence E in the period–luminosity plane. We show that their combined light and velocity curves unambiguously demonstrate that they are binaries showing ellipsoidal variability. By comparing the phased light and velocity curves of both sequence D and E variables, we show that the sequence D variation – the Long Secondary Period – is not caused by ellipsoidal variability. We also demonstrate several further differences between stars on sequences D and E. These include differences in velocity amplitude, in the distribution of eccentricity, and in the correlations of velocity amplitude with luminosity and period. We also show that the sequence E stars, unlike stars on sequence D, do not show any evidence of a mid-infrared excess that would indicate circumstellar dust.

Key words: stars: AGB and post-AGB – binaries: close – stars: oscillations

1 INTRODUCTION

Long Period Variables (LPVs) are known to fall on different sequences in the period–luminosity plane (Wood et al. 1999; Soszyński et al. 2004a; Ita et al. 2004; Fraser et al. 2005; Soszynski et al. 2007; Fraser et al. 2008). One of these sequences, known as sequence E, is thought to consist of red giants in close binary systems showing ellipsoidal variability, although this has not been unambiguously demonstrated. A small number of the binaries appear to be eclipsing and others appear to have unexpectedly eccentric orbits, based on their light curve shape (Soszyński et al. 2004b).

A star in a close binary will have its Roche Lobe distorted by the tidal influence of its orbiting companion. When the star begins to fill its Roche Lobe it takes on an elongated, or ellipsoidal shape, becoming an ellipsoidal variable. The velocity variations of such stars are dominated by the orbital motion, but light variability is caused mainly by the change in apparent surface area as the star orbits around its companion. Because of this, the light curve of an ellipsoidal variable shows two maxima and minima per orbit – two cycles for every one cycle of the velocity curve. This is an easy way to unambiguously identify ellipsoidal variables and we use this test here.

Four of the other sequences of LPVs – A, B, C’ and C – are known to harbour radially pulsating variables (Wood et al. 1999). A fifth sequence, sequence D, contains stars which show Long Secondary Periods. The origin of Long Secondary Periods (LSPs) remains something of a mystery, though several attempts have been made to discover it (Wood et al. 1999; Hinkle et al. 2002; Olivier & Wood 2003; Wood et al. 2004; Nicholls et al. 2009). Due to their overlap in the period–luminosity diagram, some authors (e.g. Soszyński et al. 2004b; Soszyński 2007) have suggested that stars on sequences D and E may be fundamentally the same – binaries showing ellipsoidal variability.

Here we study a sample of sequence E binaries. In particular we present new radial velocity data derived from VLT spectra, which we use alongside MACHO light curves. We show that the variations of stars on sequences D and E are caused by different mechanisms. Preliminary results for three stars are given in Adams et al. (2006).

2 OBSERVATIONS AND DATA REDUCTION

The observations and data reduction for this sample are the same as for our recently published sequence D sample (Nicholls et al. 2009). The spectra were taken using the FLAMES/ GIRAFFE spectrograph (Pasquini et al. 2002) on the European Southern Observatory’s Very Large
Table 1. Radial Velocities of Sequence E Stars. Stars are identified by their MACHO numbers.

| HJD    | 77.7429.189 | 77.7548.68 | 77.7672.98 | 77.7737.79 |
|--------|-------------|------------|------------|------------|
| 2954.8508 | 0.00       | 247.1836  | 270.6885  | 265.7394  |
| 3005.8604 | 0.00       | 242.5239  | 260.0903  | 258.5819  |
| 3067.6028 | 0.00       | 237.8895  | 225.7872  | 239.5893  |
| 3091.5571 | 0.00       | 238.4238  | 251.1337  | 265.9271  |
| 3280.8611 | 272.6101   | 255.7782  | 284.0382  | 244.0299  |

Figure 3. A histogram of the velocity amplitude for our sample.

3 RESULTS

Plots of phased light and velocity variations for all the stars in our sequence E sample are shown in Figs. 1 and 2. A clear doubling of the phased light curve with respect to the phased velocity curve can be seen for all stars in our sample. This behaviour unambiguously demonstrates that these stars are ellipsoidal variables. Many of the stars show lightcurves with equal maxima and unequal minima, which suggests that one end of the ellipsoid is hotter and brighter than the other. From Figs. 1 and 2 we see that the deepest minimum occurs at mean velocity during decreasing radial velocity, i.e. when the red giant is behind its companion. Therefore the inner end of the red giant ellipsoid – the end closest to the companion – is the cooler end, and the side furthest from the companion is hotter. This is most likely due to gravity darkening towards the companion.

A histogram of the velocity amplitudes of our sample is shown in Fig. 3. The majority of values lie between 15 and 55 \text{ km s}^{-1}, and the mean velocity amplitude is 43.3 \text{ km s}^{-1}.

We have made a binary fit to the velocity curves of our sequence E red giants (see section 2.5 of [Nicholls et al. 2009]). We calculated the mass function,

\[ f(m) = \frac{K^3P}{2\pi G} = \frac{m^3 \sin^3 i}{(m+M)^2}, \]

using the observed values for period \( P \) and velocity semi-amplitude \( K \) (Table 2). Using the calculated mass function of our binary fit and assuming a total system mass of 2 \( M_\odot \), we calculated an estimated companion mass for each of the stars in our sample. As expected, for most systems the companion is less massive than the red giant, but for two stars this resulted in companions with significantly higher mass than the red giant. This is unlikely since the more massive companion should evolve to the red giant stage first, and even if the current red giant was originally the less massive star, its companion would most likely now be a white dwarf of lower mass than the red giant. In these two cases we chose the total mass to be such that the red giant and its companion had equal mass. This results in higher masses for these stars (total system masses of \( \sim 4.5M_\odot \)) The mass estimates are shown in Table 2 and alongside the other parameters of the binary fit to the velocity. Here \( \gamma \) is the system velocity, \( e \) is the eccentricity, \( \omega \) is the angle of periastron, \( T \) is the date of periastron, \( a \sin i \) is the semimajor axis of the red giant’s orbit, \( f(m) \) is the mass function, \( M \) is the mass of the red giant, and \( m \) the mass of its companion. We assume \( \sin i = 1 \) when calculating the masses. The errors for each element are shown on the line below each star.

The eccentricity of a binary system is expected to decrease over time due to circularising tidal forces ([Zahn 1977]), provided no mechanism is in place that will stabilise or increase the orbital eccentricity. Thus binaries with one or more red giant components are expected to describe relatively circular orbits. We confirmed this theory by calculating the circularisation time for our stars, using the formula given in [Soker 2000]. The median circularisation time of our sample is only \( \sim 3500 \) y. For comparison, the time a 1 \( M_\odot \), \( Z = 0.008 \) red giant takes to double its radius when \( R \sim 30 \) \( R_\odot \) is \( \sim 2 \times 10^7 \) y (using the evolutionary tracks of [Girardi et al. 2000]). The value of 30 \( R_\odot \) was chosen as a typical Roche Lobe radius for these stars (see the velocity amplitude calculations given later in this section). A doubling of the radius is an estimate of the evolution time over which the tides have had time to act. Ten of the eleven stars in our sample have eccentricities \( e < 0.1 \), and the mean eccentricity of the sample is 0.07. Therefore the majority of our sample of red giant binaries have fairly circular orbits, as expected. However some sequence E stars do show confoundingly high eccentricities (see [Soszynski et al. 2004b]), and this is a problem that must be solved in the future.

The relation between velocity amplitude and period for our sample and for the sequence D sample of [Nicholls et al. 2009] is plotted in Fig. 4. In a binary system, for given masses, a longer period means a wider orbit, and thus a smaller amplitude in velocity variation. Fig. 4 shows velocity amplitude decreases with increasing period for the sequence E stars, as expected. However the sequence D stars show the same velocity amplitudes for all periods and do not follow the expected binary relation. A vivid demonstration of the disparity between these two samples is found in the region where their periods overlap. At periods between 200 and

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Figure 1. Phased MACHO blue ($M_B$) and red ($M_R$) light curves and phased radial velocity curves for our sequence E stars. The blue line shows the binary fit to the velocity curve.
Figure 2. Same as Fig. 1.
Table 2. Orbital Elements for Sequence E Stars

| Star            | $\gamma$ ($\text{km s}^{-1}$) | $K$ ($\text{km s}^{-1}$) | $e$  | $\omega$ (deg) | $T$ (HJD) | $P$ (days) | $a \sin i$ ($R_\odot$) | $f(m)$ ($M_\odot$) | $M^a$ ($M_\odot$) | $m$ ($M_\odot$) |
|-----------------|-------------------------------|---------------------------|------|----------------|------------|-------------|-------------------------|-------------------|----------------|--------------|
| 77.7429.189     | 281.40                        | 25.99                     | 0.05 | 275.38         | 3323.5     | 110.34      | 56.58                   | 0.2003            | 1.07            | 0.93         |
| ± 0.57          | ± 0.80                        | ± 0.03                    | ± 28.52 | ± 8.8         | ± 442.83   | ± 74.55     | ± 0.0285                | 1.52              | 0.48           |
| ± 0.19          | ± 0.24                        | ± 0.03                    | ± 25.63 | ± 32.9        | ± 2.22     | ± 0.0024    |                        |                   |                |
| 77.7548.68      | 247.20                        | 8.54                      | 0.07 | 170.67         | 3502.6     | 74.55       | 0.0285                  |                   |                |
| ± 0.75          | ± 1.10                        | ± 0.03                    | ± 29.11 | ± 12.3        | ± 3.42     | ± 0.0575    |                        |                   |                |
| ± 0.41          | ± 0.59                        | ± 0.02                    | ± 61.77 | ± 22.6        | ± 1.55     | ± 0.0140    |                        |                   |                |
| 77.7672.98      | 250.71                        | 32.77                     | 0.06 | 38.99          | 2989.4     | 156.13      | 100.92                  | 0.5679            | 2.27            | 2.27         |
| ± 0.41          | ± 1.10                        | ± 0.03                    | ± 29.11 | ± 12.3        | ± 3.42     | ± 0.0575    |                        |                   |                |
| ± 0.41          | ± 0.59                        | ± 0.02                    | ± 61.77 | ± 22.6        | ± 1.55     | ± 0.0140    |                        |                   |                |
| 77.7673.79      | 252.37                        | 24.01                     | 0.02 | 236.49         | 3064.4     | 131.35      | 62.30                   | 0.1887            | 1.09            | 0.91         |
| ± 0.41          | ± 0.59                        | ± 0.02                    | ± 61.77 | ± 22.6        | ± 1.55     | ± 0.0140    |                        |                   |                |
| 77.7789.152     | 255.04                        | 14.03                     | 0.05 | 198.55         | 3024.2     | 157.73      | 43.67                   | 0.0451            | 1.44            | 0.56         |
| ± 0.74          | ± 0.97                        | ± 0.08                    | ± 90.81 | ± 10.5        | ± 3.05     | ± 0.0094    |                        |                   |                |
| 77.7790.72      | 275.00                        | 15.35                     | 0.19 | 262.20         | 3326.7     | 328.79      | 97.85                   | 0.1167            | 1.22            | 0.78         |
| ± 0.83          | ± 0.92                        | ± 0.06                    | ± 13.11 | ± 10.2        | ± 6.02     | ± 0.0214    |                        |                   |                |
| 77.7791.115     | 350.88                        | 21.47                     | 0.03 | 275.04         | 3032.0     | 139.18      | 59.02                   | 0.1429            | 1.17            | 0.83         |
| ± 0.30          | ± 0.35                        | ± 0.02                    | ± 40.51 | ± 16.3        | ± 0.97     | ± 0.0070    |                        |                   |                |
| 77.7910.41      | 238.06                        | 20.41                     | 0.08 | 10.03          | 3075.8     | 191.46      | 76.94                   | 0.1673            | 1.13            | 0.87         |
| ± 0.55          | ± 0.66                        | ± 0.04                    | ± 21.82 | ± 11.8        | ± 2.53     | ± 0.0163    |                        |                   |                |
| ± 1.67          | ± 2.83                        | ± 0.04                    | ± 38.55 | ± 7.1         | ± 3.67     | ± 0.1131    |                        |                   |                |
| 77.7912.111     | 231.16                        | 14.76                     | 0.06 | 223.73         | 3075.1     | 128.89      | 37.50                   | 0.0428            | 1.44            | 0.56         |
| ± 0.45          | ± 0.62                        | ± 0.04                    | ± 41.73 | ± 14.7        | ± 1.57     | ± 0.0054    |                        |                   |                |
| 77.7914.74      | 305.31                        | 16.33                     | 0.02 | 272.80         | 3271.8     | 282.24      | 91.04                   | 0.1276            | 1.20            | 0.80         |
| ± 0.11          | ± 0.14                        | ± 0.01                    | ± 24.26 | ± 18.9        | ± 0.79     | ± 0.0033    |                        |                   |                |

$a$ Here we assume $\sin i = 1$.

Figure 4. Full velocity amplitude plotted against orbital period for our sequence E sample (blue points) and the sequence D sample of Nicholls et al. (2004) (red crosses).

450 days, the difference in velocity amplitude between the sequence D and sequence E samples is as much as 30 km s$^{-1}$.

Ellipsoidal variability is only visible once a star has substantially filled its Roche Lobe. Stars in wider orbits (with lower velocity amplitudes) will fill their Roche Lobes when they are further up the giant branch, and thus will be more luminous than stars in closer orbits. For a given luminosity (and radius) there is a range of velocity amplitudes the star may have, the maximum of which is dictated by the size of the closest possible orbit the companion can occupy. Therefore, for our ellipsoidal variables we expect that the maximum velocity amplitude should decrease with increasing luminosity, but that stars may occupy velocity amplitudes below the maximum for a given luminosity. This is shown in Fig. 5 which gives a plot of $K$ magnitude against velocity amplitude for our sequence E stars. In order to define the upper limit of velocity amplitude for a given luminosity, we calculated the minimum orbital separation for a theoretical sample of binaries with equal mass components (mass ratios of $q = 1$) in which the red giant is filling its Roche Lobe.

Using the approximation given in Eggleton (1983), we calculated the Roche Lobe radius $r_L$ to be 0.37, in units of orbital separation. Therefore the minimum orbital separation for a Roche-Lobe filling binary with $q = 1$ is $a = \frac{r_L}{2} = 2.7r_L$. We substitute for $r_L$ the radius expected for a given luminosity in these stars, calculated from a fit made to the radius–$K$ magnitude data for our sample. Finally we calculated the maximum velocity amplitude assuming a circular orbit and components of mass 1 $M_\odot$. This velocity amplitude upper limit is shown by the solid blue line in Fig. 5.

Most stars lie where expected in Fig. 5 but two stars lie above the upper limit line. These are the two systems with higher mass components, mentioned earlier. As both these systems have components of around 2.3 $M_\odot$, we also calculated the maximum velocity amplitude for stars of this mass, and this is shown by the green dashed line in Fig. 5.

One star lies above this limit. It appears somewhat atypical, as it has a significantly higher effective temperature than the rest of the sample ($\sim 5200$K compared to the median 4200K) and hence a smaller radius. It therefore does not overflow its Roche Lobe as Fig. 5 suggests.
### Table 3. Sequence E Star Properties

| Star          | $R$ ($R_\odot$) | $L$ ($L_\odot$) | $T_{\text{eff}}$ (K) | $a$ ($R_\odot$) |
|---------------|-----------------|-----------------|---------------------|-----------------|
| 77.7429.189   | 48.92           | 593.16          | 4017.43             | 121.83          |
| 77.7548.68    | 92.03           | 1917.72         | 3980.39             | 307.67          |
| 77.7672.98    | 56.13           | 869.34          | 4181.83             | 201.84          |
| 77.7673.79    | 42.24           | 591.59          | 4378.57             | 136.84          |
| 77.7789.152   | 52.85           | 841.10          | 4274.26             | 154.60          |
| 77.7990.72    | 92.71           | 1736.69         | 3868.59             | 252.27          |
| 77.7991.115   | 49.66           | 805.48          | 4362.15             | 142.23          |
| 77.7910.41    | 72.37           | 1790.14         | 4412.02             | 175.91          |
| 77.7910.77    | 38.58           | 983.43          | 5202.34             | 135.12          |
| 77.7912.111   | 47.41           | 604.76          | 4555.77             | 154.60          |
| 77.7914.74    | 70.70           | 1079.15         | 3933.14             | 227.86          |

**Figure 5.** K magnitude (from 2MASS) plotted against velocity amplitude for our sequence E stars. The point size shows relative light amplitude in MACHO red. The solid blue curve gives the upper limit for equal-mass components of 1 $M_\odot$, and the dashed green curve gives the upper limit for equal-mass components of 2.3 $M_\odot$. See text for details.

Table 3 gives the radius, luminosity, effective temperature and orbital separation data for our sample. For the majority of stars, these properties were calculated using the 2MASS $J$ and $K$ magnitudes. However for the star 77.7910.77, which lies outside the green dashed limit in Fig. 5, the properties were calculated from OGLE $V-I$ values, which are more reliable for warmer stars. Due to this star’s warmer temperature, we suspect it could be a helium core burning clump star or a blue loop star.

#### 3.1 The mid-infrared colour of sequence E stars

It has recently been shown (Wood & Nicholls 2003) that variable red giants belonging to sequence D have a mid-infrared excess when compared to similar red giants without the Long Secondary Period that characterises sequence D stars. This mid-infrared excess is assumed to arise from circumstellar dust associated with the presence of the LSP. Since the sequence E stars are close binary systems, some of which have quite eccentric orbits (Soszyński et al. 2004b), there is a possibility that these systems could have substantial circumstellar disks of dust and gas.

In order to investigate this possibility, we searched for a mid-infrared excess in sequence E stars in the LMC using mid-infrared data from the Spitzer Space Telescope SAGE survey (Blum et al. 2006; Meixner et al. 2006). The sequence E stars were obtained from the catalogue given by Fraser et al. (2008). None of these objects were detected at 24 $\mu$m in the SAGE survey but 262 were detected at 8 $\mu$m. The light curves of these 262 stars were examined and it was found that only 184 could be considered as definite sequence E stars, i.e. ellipsoidal or eclipsing binary systems. The remainder were variables whose light curve characteristics showed that they belonged to sequence D or the pulsation sequences 1 to 4 (using the notation in Fraser et al. 2008) or they were stars of indeterminate light curve type.

In order to see if the sequence E stars show a mid-infrared excess, we obtained a comparator sample of stars that were similar to the sequence E stars, but without binary companions. Such stars are the normal, non-varying field red giants in the LMC. Since the sequence E stars that were detected at 8 $\mu$m have $12.5 < K < 14$ and $0.6 < J-K < 1.4$, we selected comparison sources from the SAGE survey with these characteristics along with the requirement of an 8 $\mu$m detection. An examination of this sample of approximately 10000 objects showed that sources fainter than $K = 13.5$ were near the 8 $\mu$m faint detection limit and that this significantly biased the population of detected stars in favour of objects with a higher $K-[8]$ colour. We therefore omitted such stars and compared sequence E stars and non-varying field red giants only in the interval $12.5 < K < 13.5$. Finally, all variable stars in the catalogue of Fraser et al. (2008) were removed from the list of comparison sources. This left 144 sequence E stars and ~33000 non-varying field red giants.

The $K-[8]$ colour distributions of these two samples were then examined to search for an 8 $\mu$m mid-infrared excess. A two sample K–S test gives a probability of up to 0.89 that the sequence E stars and non-varying field red giants come from the same underlying distribution in $K-[8]$ colour. In other words, there is no evidence that sequence E variability generally leads to a significant amount of circumstellar dust and a mid-infrared excess.

### 4 DISCUSSION AND CONCLUSIONS

With new velocity curves, we now have strong evidence that the sequence E variation is indeed caused by ellipsoidal variability. This is shown by the doubling of the light curve with respect to the velocity curve in these stars, as in Figs. 1 and 2.

However, as we showed in Nicholls et al. (2009), the phased light curves of sequence D variables – the stars with Long Secondary Periods – do not show this doubling phenomenon (see fig. 3 of that paper). Although it has been suggested that the sequence D and E variations may have a common origin due to their proximity in the period–luminosity plane (Soszyński et al. 2004b), and the possible existence of ellipsoidal shapes in their residual light curves (Soszyński 2007), no sequence D star has so far been found whose light...
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executes two cycles during one velocity cycle. This seems to rule out ellipsoidal variation in sequence D stars.

A further difference between the stars on sequences D and E is demonstrated by their respective velocity amplitudes. The sequence E stars of the current sample show full velocity amplitudes of at least 15 km s$^{-1}$ – some much larger – as can be seen in Fig. 3. However as we showed in Nicholls et al. (2009), stars with LSPs have much smaller velocity amplitudes, typically around 3.5 km s$^{-1}$. This marked difference in the size of the velocity variations between sequence D and E – which can be seen in Fig. 3 – supports our assertion that they are caused by different mechanisms.

The sequence E stars, known binaries, show an expected spread in companion mass estimates. However this distribution seems very different for the sequence D stars. If treated as binaries, sequence D stars have companions that are small – as most of these stars have almost circular orbits, angle of periastron is poorly defined (see the large errors in Table 2).

The distribution of eccentricity is very different for sequence E and D stars, when the latter are treated as binaries. Most of the red giant binaries on sequence E have low eccentricity orbits, as expected for their evolutionary stage. However Nicholls et al. (2009) showed that the sequence D stars have a significantly higher eccentricity, if we assume they are binaries (the mean eccentricity of that sample is 0.3). A two-sample K-S test gives a probability of less than $2.1 \times 10^{-6}$ that the sequence D and E eccentricity distributions come from the same underlying distribution.

Further evidence that sequence D stars are not ellipsoidal variables is given by the relation between luminosity and velocity amplitude in those stars. In Fig. 4 we showed that the sequence E stars generally populate an area delineated by a maximum velocity amplitude–luminosity relation, as expected for ellipsoidal variables. However, Nicholls et al. (2009) showed that the sequence D stars do not show any correlation between these properties.

Finally, we have searched for a mid-infrared excess in sequence E stars since such an excess was found among the sequence D stars. No mid-infrared excess was found, demonstrating another difference from the sequence D stars.

In summary, we have demonstrated several significant differences between stars on sequences D and E. Most particularly, we have shown that Long Secondary Periods – the sequence D variation – are not caused by ellipsoidal variability, unlike the variation of the sequence E stars. The cause of Long Secondary Periods remains, at this time, a mystery.

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