Transparent half metallic g-C$_4$N$_3$ nanotubes: potential multifunctional applications for spintronics and optical devices

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Multifunctional material brings many interesting issues because of various potential device applications. Using first principles calculations, we predict that the graphitic carbon nitride (g-C$_4$N$_3$) nanotubes can display multifunctional properties for both spintronics and optical device applications. Very interestingly, armchair tubes ($n$, $n$) with $n = 2, 3, 4, 5, 6$ and $(5, 0)$ zigzag tubes are found to be half metallic, while zigzag tubes ($n$, 0) with $n = 4, 6$ show an antiferromagnetic ground state with band gaps. However, larger zigzag tubes of $(7, 0)$, $(8, 0)$, and $(10, 0)$ are turned out to be half metallic. Along with the half metallic behavior of the tubes, those tubes seem to be optically transparent in the visible range. Due to these magnetic and optical properties, we suggest that the g-C$_4$N$_3$ nanotubes (CNNTs) can be used for both ideal spintronics and transparent electrode materials. We also explored the stability of magnetic state and nanotube structure using ab initio molecular dynamics. The CNNTs were found to be thermally stable and the magnetic moment was robust against the structural deformation at 300 K. Overall, our theoretical prediction in one dimensional CNNTs may provide a new physics in spintronics and also in other device applications because of potential multifunctional properties.

Half metallic system is of particular interest in spintronics because one spin channel is completely suppressed at the Fermi level and due to this feature many technical difficulties for device applications can be avoided. In particular, magnetism arising from pure 2$p$ electron system without any 3$d$ transition metal elements can bring great advantage for spintronics. For instance, a spin relaxation time is one of the key factors in spintronics and it is inversely proportional to spin orbit coupling. Thus, relatively long spin relaxation time is expected from 2$p$ electron systems because of weak spin orbit coupling compared with the strength of spin orbit coupling found in conventional 3$d$ transition metal systems.

Regarding the 2$p$ magnetism, considerable efforts have been devoted towards the synthesis, characterization, and magnetism discovery in g-C$_3$N$_4$ system$^{1-4}$. However, the g-C$_3$N$_4$ was found to be non-magnetic$^{5,6}$. In 2010, a similar graphitic carbon nitride material so called g-C$_4$N$_3$ was synthesized$^7$. Recent study showed that a ferromagnetic ground state could be found in two dimensional g-C$_4$N$_3$ sheet$^8$, and several works have been reported$^{9-14}$. Since the g-C$_4$N$_3$ consists of purely 2$p$ elements, it will be of interest if one can obtain metal free half metallic state in nanotube structures and we believe that it will be possible to synthesize g-C$_4$N$_3$ nanotubes (CNNTs) using the experiences obtained from carbon nanotubes fabrication study. Indeed, one can easily find numerous studies on one dimensional g-C$_3$N$_4$ nanotubes$^{15-17}$ and these g-C$_3$N$_4$ nanotubes are found to be non-magnetic semiconductor. Unlike many studies on g-C$_3$N$_4$ nanotubes, no report has been presented so far for the possibility of metal free half metallic state and optical properties in one dimensional CNNTs systems. Herein, we show that the half metallic behavior can be observed in CNNTs and the relationship between magnetism and chirality of CNNTs are investigated as well. In addition, the thermal stability of tubular structures and robustness of ferromagnetic state at room temperature are explored using ab initio molecular dynamics. Furthermore, the frequency dependent dielectric function and energy dependent absorption coefficient for optical property are calculated. With these studies, our objective is to propose that the g-C$_4$N$_3$ nanotubes can be utilized as potential multifunctional materials for both spintronics and optical device applications.
Results

The CNNTs considered in our calculations are based on two dimensional $g\text{-C}_4\text{N}_3$ layer in the perspective of the geometry as shown in Fig. 1. The part depicted in red region is a unit cell of $g\text{-C}_4\text{N}_3$ which contains four C atoms and three N atoms. A carbon atom located out of the hexagonal ring is denoted by C*. Three other N atoms are represented by N1, N2, and N3. Fig. 2 (a)–(h) shows the optimized configurations of CNNT systems. All the tubes are found to be nearly round shape except (2, 2) armchair tube. In this particular (2, 2) armchair tube, it appears like a square with a parameter of 5.09 Å. A diameter of the tube can be determined by chirality index and an approximated diameter of tube is indicated. Besides this diameter, the length of unit cell also controls the structure of the tube. For armchair tubes, the length of one unit cell was about 4.85 Å in (2, 2) case and it is almost unchanged in other armchair tubes. In zigzag tubes, the length was 8.31 Å in both (4, 0) and (6, 0) tubes, whereas it became 8.38 Å in (5, 0). For larger tubes of (7, 0), (8, 0) and (10, 0) indices, it was 8.38 Å and these zigzag tubes whose diameter is larger than 10.7 Å show a buckling behavior as found in a two dimensional layer8.

In each structure, we considered three magnetic states such as ferromagnetic (FM), antiferromagnetic (AFM), and non-magnetic (NM) states and total energy calculations were performed. Note that the structure optimization has been performed in each spin configuration. The total energy of FM state was set to zero as a reference energy. In Table 1, we present the calculated total energy differences. First of all, the armchair CNNTs have always FM ground state. However, in small size of zigzag tubes, the magnetic ground state fluctuates as the diameter of the tube changes. For instance, both (4, 0) and (6, 0) zigzag CNNTs were found to be more stable in the AFM state than the other spin states. In contrast, the FM state was obtained in (5, 0) tube. Interestingly, we found FM ground state in (7, 0), (8, 0), and (10, 0) zigzag tubes. From the calculated results of 11 different tubes, we propose a hypothetical rule for magnetism of CNNTs. The armchair tube always prefers FM state, while the zigzag tube of $(n, 0)$ index manifests FM ground state if $n$ is larger than 6. Of course, further investigation is required to verify the rule for magnetism. We also calculated magnetic moment of each tube. In FM state, both armchair and zigzag tubes of $(n, n)$ and $(n, 0)$ indices have magnetic moment of $2n\mu_B$. Since there are $2n$ block subcells in each tube, the magnetic moment per subcell becomes $1\mu_B$. In AFM state, each subcell maintains magnetic state, but the net magnetization completely vanishes due to the opposite spin polarization in the neighboring subcells. Note that the calculated magnetic moment per cell in a two dimensional layer is $1\mu_B$. This result implies that the magnetic moment per subcell seems very robust despite dramatic changes in geometric structure. In addition, the integer magnetic moment implies that the CNNTs have half metallic characteristics. In structural point of view, the CNNT will gradually transform into two dimensional layer structure as the diameter of the tube increases and finally the CNNT will show the same magnetic property found in two dimensional layer system. In our calculations, we clearly proposed the critical diameter of tube which showed the half metallic ground state regardless of the chirality. Overall, the CNNTs show chirality independent half metallic state when the diameter of the...
tube is larger than a certain critical value and this finding will be definitely favorable for spintronics applications in various ways.

We now present the calculated spin magnetic moments of N and C atoms inside Wigner-Seitz radius of 0.863 Å for N and 0.741 Å for C, respectively in Table 2. It is observed that the spin polarization mainly originates from N atoms, whereas the C atoms do not show meaningful spin polarization, except (2, 2) armchair tube. In (2, 2) tube the carbon atom, which is located out of the hexagonal ring (C*), was found to be spin polarized and this is due to an unusual geometric feature of (2, 2) armchair tube. As depicted in Fig. 1, there are three N atoms. Both N2 and N3 atoms were found to have the same magnetic moment in FM tubes, while the three N atoms were inequivalent in AFM tubes. Very interestingly, the integer number of magnetic moment per subcell is obtained if we include the contribution to the magnetic moment from interstitial part and this implies that the system becomes half metallic material.

Fig. 3 shows the calculated electronic band structure of CNNTs. Indeed, we noticed that the band structures of (5, 5), (6, 0) and (10, 0) tubes were similar to those of (6, 6), (4, 0) and (8, 0), respectively, thus they are omitted in Fig. 3. In armchair tubes, as indicated from the calculated magnetic moment per subcell, one can clearly see half metallic state because the occupied majority band plays completely below the Fermi level, while the minority spin bands cross the Fermi level. The same half metallicity is observed in zigzag tubes as well, except for (4, 0) and (6, 0) tubes. The calculated band gaps in majority spin bands are 2.26, 1.99, 2.05, 2.11, 1.78, 2.08, 2.11, and 2.07 eV for the tubes (2, 2), (3, 3), (4, 4), (5, 5), (6, 6), (5, 0), (7, 0), (8, 0), and (10, 0) respectively. In (4, 0) and (6, 0) tubes, the band gaps are observed and they are 0.27 and 0.28 eV, respectively. Therefore, (4, 0) and (6, 0) zigzag tubes are semiconductors. In Fig. 4, we present calculated total density of states (DOS). As indicated in band structures, the DOS also clearly shows half metallic behavior in armchair tubes and (5, 0), (7, 0), and (8, 0) zigzag tubes, whereas band gap is found in (4, 0) tube. By further analyzing the calculated DOS of each tube, we have observed that the contribution to magnetism originates from p orbitals and the spin polarized orbitals depend on chirality and tube structures. Moreover, we have extracted the information on the localized orbitals which are responsible for the magnetic moment. In (3, 3), (4, 4), (5, 5) and (6, 6) armchair tubes which have cylinder shapes, both axial orbitals of N2 and N3 (equivalent to N2) atoms and tangential orbital of N1 atom mainly contribute to the magnetic moment. In (2, 2) tube, which is close to square tube, axial orbital of N2 and N3 atoms and radial orbital of C* atom mainly contribute to the magnetic moment. However, in zigzag tubes like (5, 0), (7, 0), (8, 0) and (10, 0), both axial and radial orbitals of N1 contribute to the magnetic moment. Comparing both orbitals, we found that the axial orbital contribution was relatively stronger. In N2 and N3 atoms, both tangential and axial orbitals play an essential role for the magnetism. In this case the tangential component contributed to the magnetic moment a little bit more than axial component.

To investigate the thermal stability and the existence of magnetic state, spin-polarized ab initio molecular dynamics simulations were performed at 300 K and 500 K up to 10 ps for (4, 4). The CNNT tube structures at both 300 K and 500 K are shown in Fig. 5. At 300 K, the essential tube structure is intact, even though a small distortion is observed and the magnetic state remains with an average magnetic moment of 8 μB. Note that this temperature has nothing to do with the critical temperature because the ab initio molecular dynamics does not include spin dynamics. Nonetheless, we find that the magnetic state is very robust against the structural deformation. The thermal stability at 500 K was also checked. The tube structure was deformed significantly, and it tends to convert into two connected plain surfaces due to strain of nanotube geometry. Furthermore, the subcell structure is destroyed because of large displacement of some atoms, and pentagon circles appear. The geometry is not a construction from the subcell anymore. This indicates that the tube structure is not thermally stable at 500 K.

Along with the half metallic properties found in CNNTs, the CNNTs systems will attract extensive research interest as a multifunctional material if the CNNTs can be utilized for device applications using optical properties. Thus, it will also be of interest to investigate optical properties of CNNTs. To this end, we have calculated frequency dependent dielectric function ε(ω) = ε1(ω) + iε2(ω) for optical properties. From this dielectric function, the absorption coefficient (α(E)) as a function of photon energy (E(eV)) can be obtained using the following formula:

\[ \alpha(E) = \frac{2\pi E((eV))}{\hbar c} \sqrt{\frac{\varepsilon_1^2(\omega) + \varepsilon_2^2(\omega) - \varepsilon_1(\omega)}{2}} \]  

The real and imaginary parts of dielectric function is related by well-known Kramers-Kronig relations, we thus only present imaginary part of dielectric functions in Fig. 6 (a) and (b) for both perpendicular and parallel polarization to the tube axis. Since the intensity of imaginary part of the dielectric function in parallel polarization is larger than that in perpendicular polarization, we expect optical anisotropy for absorption coefficient according to the polarization. From the band calculated structure results, one can easily find that the contribution to dielectric function due to intraband transition can be ignored if the photon energy is larger than approximately 0.5 eV. Thus, we have realized that the interband transition plays an essential role in the wide range of photon energy for the frequency dependent dielectric function. For optical device applications, it is of interest to

| Table 1 | Calculated total energy differences (in meV) of CNNTs |
|---------|---------------------------------|
| Index   | (2, 2) | (3, 3) | (4, 4) | (5, 5) | (6, 6) | (4, 0) | (5, 0) | (6, 0) | (7, 0) | (8, 0) | (10, 0) |
| FM      | 0      | 0      | 0      | 0      | 0      | −180   | 665    | −540   | 838    | 202    | 251     |
| AFM     | 250    | 370    | 460    | 601    | 807    | 0      | 0      | 0      | 0      | 0      | 0       |
| NM      | 360    | 380    | 490    | 617    | 726    | 810    | 786    | 980    | 834    | 929    | 984     |

| Table 2 | Calculated spin magnetic moment (in μB) inside Wigner-Seitz radius |
|---------|---------------------------------|
| Index   | (2, 2) | (3, 3) | (4, 4) | (5, 5) | (6, 6) | (4, 0) | (5, 0) | (6, 0) | (7, 0) | (8, 0) | (10, 0) |
| C+      | 0.24   | 0.05   | 0.03   | 0.03   | 0.03   | −0.05  | 0.05   | −0.05  | 0.10   | 0.11   | 0.02    |
| N1      | 0.08   | 0.20   | 0.24   | 0.24   | 0.25   | −0.10  | 0.29   | −0.10  | 0.28   | 0.27   | 0.26    |
| N2      | 0.22   | 0.27   | 0.26   | 0.26   | 0.26   | −0.18  | 0.23   | −0.20  | 0.24   | 0.24   | 0.25    |
| N3      | 0.22   | 0.27   | 0.26   | 0.26   | 0.26   | −0.27  | 0.23   | −0.23  | 0.18   | 0.18   | 0.26    |
focus on the absorption coefficients in the visible ranges. Using the
relation presented in the above, the energy dependent absorption
coefficients are shown in Fig. 7 (a) and (b) for both polarization
directions. The intensity of traveling light will decay exponentially
as a function of distance. Thus, one can find that the attenuation of
traveling visible light is very weak and this, in turn, implies that the
CNNTs are likely to be optically transparent. Thus, the CNNTs may
have potential applications for transparent electrode as well as spin-
tronics materials.

Discussion
We have investigated magnetic and optical properties of CNNTs by
using density functional calculations. Interestingly, the armchair
CNNTs considered in our calculations displayed half metallic
ground state. On the other hand, the zigzag tubes showed size
dependency. In (5, 0) tube, the half metallic state was found, but
the AFM state was stable in (4, 0) and (6, 0). Surprisingly, we found
half metallic ground state in larger zigzag tubes of (7, 0), (8, 0), and
(10, 0) indices. Due to lack of either theoretical or experimental
evidences for chiral dependent magnetism of CNNTs, further invest-
igation is necessary to confirm our results. Nonetheless, we have
proposed a rule for magnetism of CNNTs. The armchair tube always
prefers half metallic state. In contrast, the magnetic state of (n, 0)
zigzag tube shows the diameter dependency in small tubes, but the
zigzag tubes maintain half metallic state if the diameter is larger than
that of (6, 0) tube. These results indicate that both armchair and
zigzag tubes are likely to be half metallic, except for small tubes
and this chirality independent half metallic feature will be greatly
advantageous for spintronics applications. The ab initio molecular
dynamics simulations reveal that the magnetic tube structure is
stable at room temperature. Additionally, we have calculated the
frequency dependent dielectric functions and absorption coeffi-
cients. In general, the absorption coefficient is larger in parallel polar-
ization than in perpendicular polarization. More interestingly, we
have obtained that the CNNTs are likely to be optically transparent
in the range of visible light. This may imply that the CNNTs can be
utilized in optical devices. Overall, the theoretical prediction for half
metallicity without any external factor in one dimensional CNNTs
may lead to new physics in spintronics and also other device applica-
tions because of potential multifunctional properties.

Methods
Vienna ab initio simulation package (VASP) was used18–21. Herein, the full potential
projected plane wave framework22,23 was used with an energy cutoff of 400 eV and the
semi-local Perdew-Burke-Ernzerhof exchange-correlation functional24 was
employed. Structure optimization was performed using energy and force minimiza-
tion procedures. Thus, all atoms have been fully relaxed until the force on each
individual atom was smaller than 0.02 eV Å−1. All calculations were performed based
on using 1 × 1 × 9 k-points. The CNNTs considered in our calculations are rolled up
from two dimensional ϕ-C3N3 layer in the perspective of the geometry. A building of
CNNT has the same rule as applied for carbon nanotube. According to the labeling
rule of tubular structures of carbon nanotube25, the tube is defined by the chiral index
(n, m) based on lattice vectors. The tubes with index (n, 0) is termed zigzag tube, while
the tube labeled (n, n) is termed armchair structure. To explore the effect of chirality on

Figure 3 | Calculated energy band structures: (a)–(d) are for (2, 2), (3, 3), (4, 4) and (6, 6) armchair tubes, respectively and (e)–(h) are for (4, 0), (5, 0), (7,
0) and (8, 0) zigzag tubes, respectively. The red lines represent majority spin bands and the blacks lines are for minority spin bands. The Fermi level is
indicated in blue dashed line.
the magnetic property, we considered two types of CNNT such as armchair and zigzag structures. For zigzag CNNTs, six different structures with (4, 0), (5, 0), (6, 0), (7, 0), (8, 0), and (10, 0) are calculated and five armchair CNNTs of (2, 2), (3, 3), (4, 4), (5, 5), and (6, 6) structures are considered. The thermal stability was studied by using ab initio molecular dynamics. Here, we considered (4, 4) tube that contains 56 atoms and the molecular dynamics simulations were carried out at 300 and 500 K. Nosé–Hoover thermostat was used to control the ionic temperature. The time-step is set as 1 fs.

Figure 4 | Calculated total DOS: (a)–(d) are for (2, 2), (3, 3), (4, 4) and (6, 6) armchair tubes, respectively and (e)–(h) are for (4, 0), (5, 0), (7, 0) and (8, 0) zigzag tubes, respectively.
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Acknowledgments
This research was supported by Basic Science Research Program through the National Research Foundation of Korea (NRF) funded by the Ministry of Education, Science and Technology (No. 2013R1A1A200671) and by the Supercomputing Center/Korea Institute of Science and Technology Information with supercomputing resources including technical support (KSC-2014-C3-015).

Author contributions
T.Hu and A.Hashmi are co-first authors and equally contributed to this work. J.H. reviewed and wrote the manuscript. T.H. prepared figure 1–4 and figure 7. A.H. prepared figure 5–6.

Additional information
Competing financial interests: The authors declare no competing financial interests.
How to cite this article: Hu, T., Hashmi, A. & Hong, J.S. Transparent half metallic g-C4N3 nanotubes: potential multifunctional applications for spintronics and optical devices. Sci. Rep. 4, 6059; DOI:10.1038/srep06059 (2014).

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