Abstract

We present the first global analysis of the Constrained NMSSM that investigates the impact of the recent discovery of a 126 GeV Higgs-like boson, of the observation of a signal for branching ratio \( \text{BR}(B_s \to \mu^+\mu^-) \), and of constraints on supersymmetry from \( \sim 5\text{fb} \) of data accumulated at the LHC, as well as of other relevant constraints from colliders, flavor physics and dark matter. We consider three possible cases, assuming in turn that the discovered Higgs boson is (i) the lightest Higgs boson of the model; (ii) the next-to-lightest Higgs boson; and (iii) a combination of both roughly degenerate in mass. The likelihood function for the Higgs signal uses signal rates in the \( \gamma\gamma \) and \( ZZ \to 4l \) channels, while that for the Higgs exclusion limits assumes decay through the \( \gamma\gamma \), \( \tau\tau \), \( ZZ \) and \( W^+W^- \) channels. In all cases considered we identify the 68% and 95% credible posterior probability regions in a Bayesian approach. We find that, when the constraints are applied with their respective uncertainties, the first case shows strong CMSSM-like behavior, with the stau coannihilation region featuring highest posterior probability, the best-fit point, a correct mass of the lightest Higgs boson and the lighter stop mass in the ballpark of 1 TeV. We also expose in this region a linear relationship between the trilinear couplings of the stau and the stop, with both of them being strongly negative as enforced by the Higgs mass and the relic density, which outside of the stau coannihilation region show some tension. The second and the third case, on the other hand, while allowed are disfavored by the constraints from direct detection of dark matter and from \( \text{BR}(B_s \to \mu^+\mu^-) \). Without the anomalous magnetic moment of the muon the fit improves considerably, especially for negative effective \( \mu \) parameter. We discuss how the considered scenarios could be tested further at the LHC and in dark matter searches.
1 Introduction

In July 2012 the CMS and ATLAS collaborations at the LHC made the announcement of a $\sim 5\sigma$ discovery of a boson with mass $125.3 \pm 0.6\text{ GeV}$ \cite{1} and $126.0 \pm 0.6\text{ GeV}$ \cite{2}, respectively, consistent with the Higgs boson predicted by the electroweak (EW) Standard Model (SM). The CMS Collaboration has recently updated its results \cite{3} to $125.8 \pm 0.6\text{ GeV}$. The updated result is based on the analysis of the data corresponding to integrated luminosities of $5.1\text{ fb}$ at $\sqrt{s} = 7\text{ TeV}$ and up to $12.2\text{ fb}$ at $\sqrt{s} = 8\text{ TeV}$ in the $\gamma\gamma$, $ZZ$, $WW$, $\tau\tau$ and $bb$ decay channels. The ATLAS analysis combined approximately $4.8\text{ fb}$ of 2011 data at $\sqrt{s} = 7\text{ TeV}$ in the same five channels with $5.8\text{ fb}$ of data at $\sqrt{s} = 8\text{ TeV}$ in the $ZZ$, $\gamma\gamma$ and $WW$ channels only. Evidently, the excess of events near the reported mass is driven by the $\gamma\gamma$ and $ZZ$ channels, owing to the highest mass resolution of these channels. Both collaborations also determined the ratio $\mu(X)$ of the observed Higgs production cross section to the one predicted by the SM, in each of the mentioned Higgs decay channels $X$. An enhancement in the $\gamma\gamma$ channel was reported by ATLAS, with $\mu(\gamma\gamma) = 1.9 \pm 0.5$, as well as by CMS, with $\mu(\gamma\gamma) = 1.6 \pm 0.4$. On the other hand, the updated value of $\mu(ZZ)$ by CMS \cite{4} and ATLAS \cite{5} is, within $1\sigma$ error, SM-like.

While its exact characteristics are still being carefully examined, such a boson is not only consistent with the SM Higgs particle but can also be easily accommodated into models of new physics, particularly those based on softly broken low-energy supersymmetry (SUSY) which actually predict a relatively light Higgs boson. Most studies have been performed within the framework of the two Higgs doublet Minimal Supersymmetric Standard Model (MSSM), usually augmented by various unification boundary conditions. The framework, however, suffers from the so-called “$\mu$-problem” \cite{6}: the SUSY-preserving parameter $\mu$ in the superpotential is expected to be of the order of the SUSY breaking scale $M_{\text{SUSY}} \sim 1\text{ TeV}$ to ensure correct radiative EW symmetry breaking.

Perhaps the most compelling and simplest solution to the $\mu$-problem is to invoke an additional gauge singlet field coupled to the Higgs doublets of the MSSM \cite{6}. The $\mu$-term is then generated dynamically through the vacuum expectation value (vev) of the singlet field which is of the order of $M_{\text{SUSY}}$. The model is commonly referred to as the Next-to-Minimal Supersymmetric Standard Model (NMSSM); for reviews see, e.g., \cite{7,8}. After the discovery of the Higgs-like boson, numerous studies have appeared in the context of the NMSSM \cite{9,10,11,12,13,14,15,16}, since the model presents several interesting features. In the NMSSM the particle content remains the same as in the MSSM, except that the number of Higgs bosons increases from three to five: three neutral scalars $h_{1,2,3}$ and two neutral pseudoscalars $a_{1,2}$. The number of neutralinos also increases from four to five, $\chi_{1,\ldots,5}$, owing to the singlino partner of the singlet Higgs boson.

On the phenomenological front, a two-loop theoretical upper bound on the mass of the lightest $CP$-even Higgs boson, $m_{h_1}$, can increase by a few GeV compared to the MSSM for some combinations of the model’s parameters. Moreover, in the context of the recent LHC results, the next-to-lightest $CP$-even Higgs boson of the model, $h_2$, could also have mass around 126 GeV with $h_1$ being even lighter than the LEP bound on the SM-like Higgs boson mass, without violating it \cite{9,10}, owing to the singlet-doublet mixing effects. Both features potentially allow us to achieve the correct mass of the experimentally detected Higgs without excessive fine-tuning \cite{17,18,19,20}, making the NMSSM potentially a more “natural” model than the MSSM. Finally, the NMSSM also offers the additional possibility that the observed excess in the $\gamma\gamma$ and $ZZ$ rates could be due to the combination of $h_1$ and $h_2$ decays (with $m_{h_1}$ and $m_{h_2}$ being almost degenerate) \cite{12}. Besides masses, the decay rates of the Higgs bosons are also affected by the modifications in the superpotential. For example, for large doublet-singlet mixing, the $h_1 bb$ coupling becomes suppressed, reducing the total decay width. As a result, the branching ratio (BR) of $h_1 \rightarrow \gamma\gamma$ becomes marginally enhanced compared to the SM or the MSSM \cite{21}. An important consequence of this feature is that $h_1$ lighter...
than 115 GeV could have escaped detection at LEP, and also at the LHC, due to the possibility of its decay into a pair of the two lighter pseudoscalars, $h_1 \rightarrow a_1 a_1$ (see, e.g., [22]), causing thus a suppression in all of the other BR’s of $h_1$.

The NMSSM in its most general form contains more than a hundred free parameters: those appearing in the MSSM and some additional ones relating to the extended Higgs sector. Similarly to the MSSM, where imposing universality conditions on the soft SUSY-breaking parameters of the model at the scale of grand unification (GUT scale) leads to the Constrained MSSM (CMSSM) [23], a GUT-constrained version of the NMSSM (CNMSSM) [24, 25, 26] can be defined; see Sec. 2 for more details and discussion.

It is well known that in the CMSSM the lightest Higgs boson’s mass, as calculated at two-loop level with FeynHiggs [27] or SOFTSUSY [28], is typically a few GeV below 126 GeV, which can be considered as somewhat unsatisfactory even if one takes into account a residual error of some 2–3 GeV [29] from scheme dependence. (Values of $m_h$ around 126 GeV can still be obtained in the CMSSM for $M_{\text{SUSY}} \gg 1$ TeV at the expense of increased fine-tuning [30].) A priori one could expect that in the CNMSSM, with more freedom in the Higgs sector, the tension will be reduced. However, recent studies [16] using random scans with fixed-window application of the constraints have shown that in the CNMSSM it is extremely difficult to obtain a Higgs boson as heavy as 126 GeV, particularly one with an enhanced $\gamma \gamma$ decay rate, while also satisfying other phenomenological constraints, thus nullifying the noted advantages of the singlet-extension of the MSSM.

On the other hand, it has been demonstrated by our recent global analysis of the CMSSM [30] and by some earlier Bayesian studies [31, 32] that a proper treatment of the experimental constraints through a likelihood function can lead to significantly different results from “top-hat” scans where such constraints are typically implemented in a more simplified boxlike fashion, with all points accepted when satisfying experimental values within some fixed range (typically within 2σ), and otherwise rejected. One of the main advantages of the statistical approach is that scanned points are instead “weighted” by the total $\chi^2$, thus indicating how well they fit all constraints. For example, in the top-hat approach a point giving a value of even one constraint slightly beyond the allowed range while reproducing central values of all the other constraints would be rejected, while a point with values for all the constraints barely within the allowed boxes would be completely allowed. In contrast, in a statistical approach both points would be accepted but weighted with their respective $\chi^2$. Another advantage of the statistical approach based on the likelihood function is that theoretical and experimental uncertainties can be easily implemented in a consistent manner. Thanks to some recent developments in sampling algorithms (see, e.g., [33] and [34]), multidimensional Bayesian scans can now be carried out rather quickly and efficiently.

One should note two important changes in the data that have recently taken place on the experimental front. In November 2012 the LHCb Collaboration published the most recent update of their search for the rare decay $B_s \rightarrow \mu^+ \mu^-$ [35], reporting an excess of $B_s \rightarrow \mu^+ \mu^-$ candidates over the background. The measured value, $\text{BR}(B_s \rightarrow \mu^+ \mu^-) = 3.2^{+1.5}_{-1.2} \times 10^{-9}$, is now very close to the time-averaged SM value, $3.5 \times 10^{-9}$ [36, 37]. We include the constraint in our likelihood function taking into account both theoretical and experimental uncertainties, as will be described below.

The other important update was the top pole mass by the Particle Data Group, obtained from an average of data from Tevatron and the LHC at $\sqrt{s} = 7$ TeV, $M_t = 173.5 \pm 1.0$ GeV [38]. As we shall see below this is a welcome increase relative to its previous value in the context of the Higgs sector of constrained SUSY models as it pushes the mass of $h_1$ up, closer to the experimentally observed Higgs-like resonance mass.

In this article, we present the first global Bayesian analysis of the CNMSSM after the observation
of the SM Higgs-like boson. We separately consider the cases of this boson being $h_1$, or $h_2$, or a combination of both. We test the parameter space of the model against the currently published, already stringent constraints from SUSY searches at the LHC and other relevant constraints from colliders, $b$-physics and dark matter (DM) relic density. Our goal is to map out the regions of the parameter space of the CNMSSM that are favored by these constraints. As in our CMSSM study, the CMS razor limit based on 4.4/fb of data is implemented through an approximate but accurate likelihood function. We also study the effects of relaxing the $(g-2)_\mu$ constraint.

The article is organized as follows. In Sec. 2 we briefly revisit the model, highlighting some of its salient features. In Sec. 3 we detail our methodology, including our statistical approach and our construction of the likelihoods for the BR ($B_s \rightarrow \mu^+\mu^-$) signal, the CMS razor 4.4/fb analysis, and the CMS Higgs searches. In Sec. 4 we present the results from our scans and discuss their novel features. We summarize our findings in Sec. 5.

2 The NMSSM with GUT-scale universality

The NMSSM is an economical extension of the MSSM, in which one adds a gauge-singlet superfield $S$ whose scalar component couples only to the two MSSM Higgs doublets $H_u$ and $H_d$ at the tree level. The scale-invariant superpotential of the model has the form

$$ W = \lambda S H_u H_d + \frac{\kappa}{3} S^3 + \text{(MSSM Yukawa terms)}, $$

where $\lambda$ and $\kappa$ are dimensionless couplings. Upon spontaneous symmetry breaking, the scalar Higgs field $S$ develops a vev, $s \equiv \langle S \rangle$, and the first term in Eq. (1) assumes the role of the effective $\mu$-term of the MSSM, $\mu_{\text{eff}} = \lambda s$. The soft SUSY-breaking terms in the Higgs sector are then given by

$$ V_{\text{soft}} = m^2_{H_u} |H_u|^2 + m^2_{H_d} |H_d|^2 + m^2_S |S|^2 + \left( \lambda A_{\lambda} S H_u H_d + \frac{1}{3} \kappa A_{\kappa} S^3 + \text{h.c.} \right), $$

where $A_\lambda$ and $A_\kappa$ are soft trilinear terms associated with the $\lambda$ and $\kappa$ terms in the superpotential. The vev $s$, determined by the minimization conditions of the Higgs potential, is effectively induced by the SUSY-breaking terms in Eq. (2), and is naturally set by $M_{\text{SUSY}}$, thus solving the $\mu$-problem of the MSSM.

We define the CNMSSM in terms of five continuous input parameters and one sign,

$$ m_0, m_{1/2}, A_0, \tan \beta, \lambda, \text{sgn}(\mu_{\text{eff}}), $$

where unification conditions at a high scale require that all the scalar soft SUSY-breaking masses in the superpotential (except $m_S$) are unified to $m_0$, the gaugino masses are unified to $m_{1/2}$, and all trilinear couplings, including $A_\lambda$ and $A_\kappa$, are unified to $A_0$. This leaves us with two additional free parameters: $\lambda$ and the singlet soft-breaking mass $m^2_S$. The latter is not unified to $m^2_0$ for both theoretical and phenomenological reasons. From the theoretical point of view, it has been argued that the mechanism for SUSY breaking might treat the singlet field differently from the other superfields. From the phenomenological point of view, the freedom in $m_S$ allows for easier convergence when the renormalization group equations (RGEs) are evolved from the GUT scale down to $M_{\text{SUSY}}$. It also yields, in the limit $\lambda \rightarrow 0$, and with $\lambda s$ fixed, effectively the CMSSM plus a singlet and singlino fields that both decouple from the rest of the spectrum. Through the minimization equations of the Higgs potential, $m^2_S$ can then be traded for $\tan \beta$ (the ratio of the vev’s

\footnote{For simplicity we will be using the same notation for superfields and their bosonic components.}
of the neutral components of the $H_u$ and $H_d$ fields) and either $\text{sgn}(\mu_{\text{eff}})$ or $\kappa$. We choose $\text{sgn}(\mu_{\text{eff}})$ for conventional analogy with the CMSSM. Both $\lambda$ and $\tan \beta$ are defined at $M_{\text{SUSY}}$. Our choice of the parameter space is the same as the one used by one of us in a previous Bayesian analysis [31], of which this paper is, in some sense, an update. Of course, there exist different possibilities that have been explored in the literature. Some authors have studied the more constrained version of the CNMSSM, characterized by $m_2 = m_0$ [26]. But it is also true that the underlying assumption employed here, of a different treatment of the singlet field by the SUSY breaking mechanism, would allow for freedom in $A_\kappa$ at the GUT scale [39]. We will give some comment in the Conclusions about the possible impact of relaxing the unification condition for $A_\kappa$.

3 Statistical treatment of experimental data

We explore the parameter space of the model with the help of Bayesian formalism. We follow the procedure outlined in detail in our previous papers [40, 41, 30], of which we give a short summary here. Our aim is to map out the 68% and 95% credible regions of $p(m|d)$, the posterior probability density function (pdf), given by Bayes’ theorem,

$$p(m|d) = \frac{p(d|\xi(m))\pi(m)}{p(d)}.$$  (4)

$p(d|\xi(m)) \equiv \mathcal{L}$ is the likelihood function, which describes the probability of obtaining the data $d$ given the computed value of some observable $\xi(m)$, which is a function of the model’s parameters $m$. $\mathcal{L}$ also incorporates the experimental and theoretical uncertainties. Prior probability $\pi(m)$ encodes assumed range and distribution of $m$. Finally, $p(d)$ is the evidence, which is a normalization constant as long as only one model is considered, but serves as a comparative measure for different models or scenarios.

Bayes’ theorem provides an efficient and natural procedure for drawing inferences on a subset of $r$ specific model parameters (including nuisance parameters), or observables, or a combination of both, which we collectively denote by $\psi_i$. They can be obtained through marginalization of the full posterior pdf, carried out as

$$p(\psi_{i=1,\ldots,r}|d) = \int p(m|d)d^{n-r}m,$$  (5)

where $n$ is the total number of input parameters. An analogous procedure can be performed with the observables and with a combination of the model’s parameters and observables.

In order to evaluate the posterior probability given by Eq. (4), one needs to first construct the likelihood function. The constraints that we include in the current analysis are listed in Table 1. We shall be discussing them in turn below. As a rule, following the procedure developed earlier [49], we implement positive measurements through the usual Gaussian likelihood, while upper or lower limits through an error function smeared with both theory and, when available, experimental error. The construction of the likelihoods for direct SUSY and Higgs searches is more involved, and will be explained in detail later in this section.

3.1 Likelihood for $\text{BR}(B_s \to \mu^+\mu^-)$

In November 2012 the LHCb Collaboration published the most recent update of their search for the rare decay $B_s \to \mu^+\mu^-$ [35], based on a combination of the 2012 data samples of 1.1/fb of proton-proton collisions at $\sqrt{s} = 8$ TeV and the 2011, 1.0/fb data at $\sqrt{s} = 7$ TeV. The data superseded the combination of 2011 data from ATLAS, CMS and LHCb published in June 2012 [50].
| Measurement                  | Mean or range | Error (Exp., Th.) | Distribution | Ref. |
|------------------------------|---------------|-------------------|--------------|------|
| CMS razor 4.4/fb            | See text.     | See text.         | Poisson      | 42   |
| $m_{h_{	ext{sig}}}$        | 125.8 GeV     | 0.6 GeV, 3 GeV    | Gaussian     | 3    |
| $R_{h_{	ext{sig}}} (\gamma \gamma)$ | 1.6           | 0.4, 15%         | Gaussian     | 4    |
| $R_{h_{	ext{sig}}} (ZZ)$   | 0.80          | +0.35 – 0.28, 15%| Gaussian     | 4    |
| $m_{h_{	ext{hid}}} (\text{GeV})$ | < 122.7 GeV, > 128.9 GeV | 0, 3 GeV | 0, 15% | Error Fn | See text. |
| $R_{h_{	ext{hid}}} (\gamma \gamma, ZZ, \tau \tau, WW)$ | See text. | See text. | Gaussian | 47   |
| $\Omega B$                   | 0.1120        | 0.0056, 10%       | Gaussian     | 44   |
| $\delta (g - 2)^{\text{USY}} \times 10^{10}$ | 28.7          | 8.0, 1.0          | Gaussian     | 45, 46 |
| BR ($B \rightarrow X_{\gamma} \gamma$) $\times 10^{4}$ | 3.43          | 0.22, 0.21        | Gaussian     | 47   |
| BR ($B_{u} \rightarrow \tau \nu \times 10^{4}$) | 1.66          | 0.66, 0.38        | Gaussian     | 48   |
| $\Delta M_{B_s}$             | 17.719 ps$^{-1}$ | 0.043 ps$^{-1}$, 2.400 ps$^{-1}$ | Gaussian | 48   |
| BR ($B_{s} \rightarrow \mu^{+} \mu^{-}$) | $3.2 \times 10^{-9}$ | +1.5 – 1.2, 10% | Gaussian | 55   |

Table 1: The experimental constraints that we apply to constrain model parameters. $m_{h_{	ext{sig}}}$, $m_{h_{	ext{hid}}}$, $R_{h_{	ext{sig}}}$ and $R_{h_{	ext{hid}}}$ are defined in Sec. 3.3.

LHCb observed an excess of $B_{s} \rightarrow \mu^{+} \mu^{-}$ candidates over the background, consistent with the SM expectation. The measured value is BR ($B_{s} \rightarrow \mu^{+} \mu^{-}$) = $3.2^{+1.5}_{-1.2} \times 10^{-9}$, with a statistical significance of 3.5$\sigma$. We used this information to construct an approximate likelihood function for BR ($B_{s} \rightarrow \mu^{+} \mu^{-}$) which parameterizes the experimental and theoretical uncertainties. The most important sources of theoretical uncertainty are the $B_{s}$ decay constant (main contribution) and its lifetime, the top quark mass and the CKM matrix elements $V_{tb}^{*}V_{ts}$ and their total amounts to approximately 11% of the mean value [51]. Thus, we parametrized the likelihood function as a combination of two half-Gaussians, to take into account the asymmetry in the experimental uncertainty. A theoretical uncertainty equal to 10% of the calculated value was added in quadrature. Notice that we neglected the uncertainty due to the top pole mass ($\sim 1\%$) since it is taken care of by scanning over the SM nuisance parameters (see below).

### 3.2 Limits on SUSY from the LHC

In Ref. [30] we derived a methodology for constructing an approximate likelihood map that reproduced the lower limit in the ($m_0$, $m_{1/2}$) plane set by the CMS Collaboration with the razor method [32, 42] based on 4.4/fb of data. We did so by applying the razor method to simulated SUSY searches in all-hadronic modes. We validated our map against the experimental results by evaluating the resulting 95% C.L. contour in the ($m_0$, $m_{1/2}$) plane and comparing it with the corresponding 95% C.L. exclusion limit from the hadron box provided by the CMS Collaboration. We obtained a very good agreement confirming that our procedure for generating these likelihood maps was indeed correct. Our methodology can be applied to produce the SUSY exclusion limits in any $R$-parity conserving supersymmetric model, as long as the supersymmetric spectra in that model present similar features to the ones of the CMSSM, namely a sufficient mass difference between the lightest SUSY particle (LSP) and gluinos or squarks of the first two generations. When extending the procedure to other models, one should also take into account possible changes in the production and decay modes of the particles. In this paper we follow the same methodology for generating a SUSY likelihood map based on the CMS razor 4.4/fb analysis for the NMSSM.

For each point in an $m_0 - m_{1/2}$ grid, with 50 GeV step size in both parameters, the supersymmetric mass spectrum and decay table are generated using NMSSMTools [53], and fed into Herwig++ [54] for parton shower generation and calculation of the cross sections. Herwig++ allows one to work in the framework of the NMSSM, and hence takes care of a possible contribution
The 95% C.L. lower bounds from our approximate razor likelihood, for different values of $\lambda$ and $A_\kappa$, compared with the experimental line (in dashed black).

from the extended neutralino and Higgs sectors. The production modes are not influenced by these sectors, since the razor search is designed to detect squarks and gluinos, which are produced through color interactions. The output of Herwig++ is passed in HepMC \cite{55} format to Delphes \cite{56} for reconstruction of the physical objects by simulating the CMS detector’s response. The output from Delphes is distributed into 38 bins, defined in terms of the razor variables $M_R$ and $R^2$, each containing the data (a number of background and signal events) from the CMS-provided hadron box, to produce an efficiency map for each bin, which is then translated into a likelihood map for the whole grid. We refer the reader to Ref. \cite{30} for more details of the complete procedure adopted for the production of efficiency maps.

The 95% C.L. razor contour thus reproduced is shown in Fig. 1. The actual 95% C.L. line obtained by CMS is also shown as a dashed black line (we point out that the actual official line and the one obtained by CMS using the hadron box only are very close to each other). The relevant CNMSSM parameters were fixed as $\tan \beta = 5$, $A_0 = 0$, $A_\kappa = -15\text{GeV}$, $\lambda = 0.001$ and $\text{sgn}(\mu_{\text{eff}}) = +1$. The produced line is indicated in purple. One can see that the CMS limit is reproduced very well in the limits of $m_{1/2} \gg m_0$ and vice versa. A slight discrepancy in between those two extremes is basically irrelevant, as we shall see below. The dependence of the limit on $\lambda$ and $A_\kappa$ is negligible, since these parameters only affect the boundaries of the physically allowed region but do not cause a shift in the position of the contour. This is clear from Fig. 1 where we show a contour for $\lambda = 0.1$ (in green) and another for $A_\kappa = -1000\text{GeV}$ (in red), fixing the other parameters to the stated value in each case. The negligible dependence of the razor limit on $A_0$, $\tan \beta$ and $\text{sgn}(\mu_{\text{eff}})$ has already been verified in many analyses; see e.g., \cite{57,58,30}. Our choice of these parameters thus only ensures the maximum allowed physical region in the $(m_0, m_{1/2})$ space, since the physicality aspect is later taken into account during the scan when the unphysical points are discarded.
3.3 Likelihood for the Higgs bosons

The measured mass of the Higgs-like boson has important consequences for global properties of the CNMSSM.

An absolute upper bound on the mass of a SM-like $h_1$ can be obtained in the limit $\kappa s \gg |A_\lambda|, |A_\kappa|$ (for which the singletlike scalar becomes very heavy) and is given by

$$m_{h_1}^2 \leq M_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta - \frac{\lambda^2}{\kappa^2} v^2 \left[ \lambda - \sin 2\beta \left( \frac{A_\lambda}{2s} \right) \right]^2 + \Delta m_{h_1}^2,$$

where $\Delta m_{h_1}^2$ denotes loop corrections, and $v = 174$ GeV is the tree-level Higgs doublet vev. The second, NMSSM-induced term on the right-hand side of Eq. (6) can enhance the $h_1$ mass by a few GeV beyond its MSSM value, if $\lambda$ is large enough, $\lambda \gtrsim 0.5$, and $\tan \beta \lesssim 2$. For larger values of $\tan \beta$, the second term on the right-hand side becomes suppressed, and the third, negative term becomes significant. Then, the value of the Higgs boson mass can only be enhanced by the loop corrections. As we shall see, when other constraints are taken into account, especially the ones coming from the LEP Higgs searches, $b$-physics, the muon anomalous magnetic moment, $(g - 2)_\mu$, and DM relic density, the aforementioned conditions on $\lambda$ and $\tan \beta$ become hard to satisfy and drastically restrict the parameter space of the model.

As noted in the Introduction, in the NMSSM either of the two lightest $CP$-even Higgses could serve the role of the SM-Higgs-like boson observed at the LHC. There are thus three interesting possibilities entailing such a discovery:

Case 1: $m_{h_1} \approx 125.8$ GeV,
Case 2: $m_{h_2} \approx 125.8$ GeV,
Case 3: $m_{h_1} \approx m_{h_2} \approx 125.8$ GeV.

3.3.1 Mass likelihood

In this paper we analyze all three cases mentioned above. We will henceforth refer to our selected 125.8 GeV signal Higgs for either of the first two cases generically as $h_{\text{sig}}$. We impose a mass requirement on $h_{\text{sig}}$ through a Gaussian likelihood which takes into account both the theoretical ($\tau$) and experimental ($\sigma$) errors, following the procedure detailed in Ref. [30],

$$L_{\text{Higgs mass}}(m_{h_{\text{sig}}}) = \exp \left[-\frac{1}{2}(125.8 \text{ GeV} - m_{h_{\text{sig}}})^2 / (\tau^2 + \sigma^2) \right].$$

The theoretical error is due to residual differences between calculations using different approaches and schemes, and it is estimated in the literature to be of the order of 2–3 GeV [60]. We assume $\tau = 3$ GeV. We use the CMS determination of the Higgs mass rather than the one by ATLAS, since it has been most recently updated, and also for consistency with our previous work [30].

3.3.2 Cross section likelihood

In order to be thoroughly consistent with the CMS measurement, we need to calculate for both Higgs bosons $h_{1,2}$ the reduced cross sections, defined in the literature as

$$R_{h_i}(X) = \frac{\sigma(pp \rightarrow h_i)}{\sigma(pp \rightarrow h_{\text{SM}})} \times \frac{BR(h_i \rightarrow X)}{BR(h_{\text{SM}} \rightarrow X)},$$

We assume that the third $CP$-even Higgs is always heavier than the current experimental reach.
for a given Higgs decay channel, $X$.

Equation (8) can be approximated by

$$
R_{h_i}(X) = \sum_{Y \in \text{prod}} R^Y_{h_i}(X) R_{\text{SM}}(Y),
$$

(9)

where the sum runs over the Higgs production channels $Y$ ($Y = gg$ for gluon-fusion, $VV$ for vector boson-fusion and Higgs-strahlung off a $Z$ boson, $tt$ and $bb$ for associated Higgs production with top and bottom quarks, respectively), and the ratios $R_{\text{SM}}(Y) = \sigma(pp \rightarrow Y \rightarrow h_{\text{SM}})/\sigma(pp \rightarrow h_{\text{SM}})$ are obtained from the public tables provided by the LHC Higgs Cross Section Working Group [61, 62] for $\sqrt{s} = 8$ TeV.

The reduced cross sections $R^Y_{h_i}(X)$ for the individual production channels are provided by the mass spectrum generator included in the NMSSMTools package, which we use for our analysis. Alternatively, they can be expressed in terms of the Higgs reduced couplings $C(X)$ (the ratio of the couplings of the Higgs boson with a given mass to a pair of $X$ particles in the NMSSM, to the ones calculated in the SM) and the decay branching ratios $\text{BR}(h_i \rightarrow X)$, which are also provided by the mass spectrum generator,

$$
R^Y_{h_i}(X) \equiv \frac{\sigma(Y \rightarrow h_i)}{\sigma(Y \rightarrow h_{\text{SM}})} \times \frac{\text{BR}(h_i \rightarrow X)}{\text{BR}(h_{\text{SM}} \rightarrow X)}
$$

$$
= \frac{C^2(Y) \times \Gamma(h_i \rightarrow X)/\Gamma_{\text{tot}}}{\Gamma(h_{\text{SM}} \rightarrow X)/\Gamma_{\text{SM tot}}} \sum_{F \in \text{SM decay}} \frac{\text{BR}(h_i \rightarrow F)}{C^2(F)},
$$

(10)

where the sum runs over the decay channels $F$ open to the SM Higgs boson.

We require $R_{h_{\text{sig}}(\gamma\gamma)}$ and $R_{h_{\text{sig}}(ZZ)}$ to comply with the measured rates, $R_{\text{obs}}(\gamma\gamma) = 1.6 \pm 0.4$ [11] and $R_{\text{obs}}(ZZ) = 0.8^{+0.35}_{-0.28}$ [4], respectively. For the $\gamma\gamma$ channel the “signal” likelihood is taken to be a Gaussian around the measured central value,

$$
\mathcal{L}_{\text{sig}}(\gamma\gamma) = \exp \left[ -\frac{(R_{\text{obs}}(\gamma\gamma) - R_{h_{\text{sig}}(\gamma\gamma)})^2}{2\sigma_{\gamma\gamma}^2 + \sigma_{\gamma\gamma}^2} \right],
$$

(11)

with $\sigma_{\gamma\gamma}$ being the experimental error. For the $ZZ$ channel, since the experimental error is asymmetric, the signal likelihood is defined in terms of half-Gaussians for the positive error $\sigma_{ZZ}^+$ and negative error $\sigma_{ZZ}^-$ each, as done in the case of the $B_s \rightarrow \mu^+\mu^-$ likelihood above. $\tau_X = 15\% \times R_{h_{\text{sig}}}(X)$ is a very conservative estimate of the theoretical error based on [63], used for every channel $X$.

In addition to constraining $h_{\text{sig}}$, there is another crucial aspect of cases 1 and 2, which is that the second of the two lightest $CP$-even Higgs bosons must have escaped detection at the LHC (or at LEP if very light), or be “hidden.” In the following we refer to it as $h_{\text{hid}}$. In other words, the production rate of $h_{\text{hid}}$ should be less than what the experiments are currently sensitive to for all $X$. As a result, $R_{h_{\text{hid}}}(X)$ should also be constrained by experimental data, so that all points where the rate of $h_{\text{hid}}$ is large enough for it to have been observed are rejected in our analysis. For this purpose, we construct an “exclusion” likelihood. Following the procedure outlined in [49] for exclusion bounds we first define a step function,

$$
\mathcal{L}_{\text{excl}}^{(\text{step})}(m_{h_{\text{hid}}}, R_{h_{\text{hid}}}(X), \mu_{95}(X)) = \begin{cases} 
1 & \text{for } R_{h_{\text{hid}}}(X) \leq \mu_{95}(X) \\
0 & \text{for } R_{h_{\text{hid}}}(X) > \mu_{95}(X),
\end{cases}
$$

(12)

We only use the dominant decay channels where a $\sim 5\sigma$ excess has been observed.
where \( \mu_{95}(X) \) is the value of the signal strength modifier \( \mu(X) \equiv \sigma_{h_{\text{hid}}}(X)/\sigma_{h_{\text{SM}}}(X) \) that is excluded at 95\% C.L. by the LHC searches for a Higgs with a given mass \( m_H = m_{h_{\text{hid}}} \) obtained from the latest exclusion plots published by the CMS Collaboration \( [63] \). The LEP exclusion limits are taken into account by NMSSMTools beforehand.

Then, in order to include the theoretical error on the true values of the reduced cross section and the Higgs mass, \( L_{\text{excl}}^{(\text{step})} \) is smeared out further by convolving it with Gaussian functions centered around their true theoretical values \( \hat{R}_{h_{\text{hid}}}(X) \) and \( \hat{m}_{h_{\text{hid}}} \), respectively, so that the exclusion likelihood now becomes

\[
L_{\text{excl}}^{(\text{smear})}(m_{h_{\text{hid}}}, R_{h_{\text{hid}}}, \mu) = \int d\hat{m}_{h_{\text{hid}}} \int d\hat{R}_{h_{\text{hid}}} L_{\text{excl}}^{(\text{step})}(\hat{m}_{h_{\text{hid}}}, \hat{R}_{h_{\text{hid}}}, \mu) \times \exp\left[ -\frac{(\hat{m}_{h_{\text{hid}}} - m_{h_{\text{hid}}})^2}{2\tau^2} \right] \exp\left[ -\frac{(\hat{R}_{h_{\text{hid}}} - R_{h_{\text{hid}}})^2}{2\bar{\tau}^2} \right],
\]

where the theoretical errors are taken to be \( \tau = 3 \text{ GeV} \) and \( \bar{\tau} = 15\% \cdot R_{h_{\text{hid}}} \) \( [63] \), respectively. The exclusion likelihood is calculated for \( X = \gamma\gamma, ZZ, WW \) and \( \tau\tau \). Finally, in order for our exclusion criterion to be consistent with our criterion for signal observation at \( 125.8 \pm 3.1 \text{ GeV} \) (with theory and experimental errors added in quadrature), we further impose the condition

\[
L_{\text{excl}}(X) = \begin{cases} 0 & \text{for } 122.7 \text{ GeV} \leq m_{h_{\text{hid}}} \leq 128.9 \text{ GeV} \\ L_{\text{excl}}^{(\text{smear})}(X) & \text{elsewhere}. \end{cases}
\]

For case 3, the likelihood in Eq. (7) is separately computed for both \( h_1 \) and \( h_2 \). In this scenario, only the combined production rate for \( h_1 \) and \( h_2 \) needs to be equal to \( R_{\text{obs}}(X) \). Hence the observation likelihood is now defined as

\[
L_{\text{obs}}(X) = \exp\left\{-\frac{[R_{\text{obs}}(X) - (R_{h_1}(X) + R_{h_2}(X))]^2}{2(\sigma_X^2 + \tau_X^2)}\right\}.
\]

The values and uncertainties of our Higgs constraints are given in Table 1.

### 4 Methodology and Results

The scanned ranges of the CNMSSM parameters along with the type of distribution of their prior are listed in Table 2. Also listed in the table are the input ranges of the nuisance parameters included in the scans. The sign of \( \mu_{\text{eff}} \) is fixed to +1 or −1 for a given scan.

The reason for choosing the given range of \( \lambda \) is twofold. First, we have checked that allowing lower values of \( \lambda \) hardly increases the number of points allowed by the physicality conditions. Second, allowing very small values of \( \lambda \) would have most likely driven the scan towards a purely CMSSM-like scenario, thus preventing us from scrutinizing any characteristic features of the CNMSSM, particularly for case 1.

The analysis was performed using the package BayesFITS which engages several external, publicly available tools: for sampling it uses MultiNest \( [65] \) with 4000 living points, evidence tolerance factor set to 0.5, and sampling efficiency equal to 0.8. Mass spectrum, along with \( \Delta M_{B_S} \), is computed with NMSSMTools v3.2.1 \( [53] \) and passed via SUSY Les Houches Accord format to SuperIso

---

4 We used the latest exclusion limits provided based on 5.1/fb of data at \( \sqrt{s} = 7 \text{ TeV} \) and 12.2/fb of data at \( \sqrt{s} = 8 \text{ TeV} \) for the \( ZZ \) channel, on 4.9/fb at \( \sqrt{s} = 7 \text{ TeV} \) and 12.1/fb at \( \sqrt{s} = 8 \text{ TeV} \) for the \( WW \rightarrow ll\nu\nu \) channel and on 17/fb at \( \sqrt{s} = 7 - 8 \text{ TeV} \) for the \( \tau\tau \) channel. Limits for the \( \gamma\gamma \) channel have not been updated by CMS and are, therefore, still based on a combination of 5.1/fb at \( \sqrt{s} = 7 \text{ TeV} \) and 5.3/fb at \( \sqrt{s} = 8 \text{ TeV} \) of data.
Table 2: Priors for the parameters of the model and for the SM nuisance parameters used in our scans. Masses and $A_0$ are in GeV.

v3.3 [66] to calculate BR ($B \rightarrow X_s \gamma$), BR ($B_s \rightarrow \mu^+ \mu^-$), BR ($B_d \rightarrow \tau \nu$), and $\delta (g-2)^{\mu}_{\text{SUSY}}$. DM observables, such as the relic density and direct detection cross sections, are calculated with MicrOMEGAs 2.4.5 [67].

Below we will present the results of our scans as one-dimensional (1D) or two-dimensional (2D) marginalized posterior pdf maps of parameters and observables. For example, in evaluating a posterior pdf for a given parameter, we marginalize over all of the model’s other parameters and the SM nuisance parameters, as described in detail in Refs. [30, 41].

Notice that when discussing the results of the global scan for case 1 it will become apparent that this case presents a remarkable CMSSM-like behavior. It would therefore be natural to try to compare those results with our recent CMSSM analysis [30]. In doing so, one needs to take into account the differences between the numerical codes and constraints adopted in both studies. We summarize them here.

1. In the present study we use NMSPEC (included in NMSSMTools) for calculating the supersymmetric spectrum, while in [30] we used SOFTSUSY. We have repeatedly cross-checked the spectra obtained in the MSSM limit of the NMSSM with the ones generated by SOFTSUSY, finding some differences, especially with respect to loop corrections giving the largest values of the lightest Higgs mass. In some regions of the parameter space the difference between the two generators can amount to a maximum of $\sim 0.5$–1 GeV. Given the experimental and theoretical uncertainties in the Higgs mass, such difference translates into $\sim 0.25$ units of $\chi^2$, which is not significant for the purpose of the global scan.

2. In this paper we use the value of BR ($B_s \rightarrow \mu^+ \mu^-$) measured at LHCb [35], which has been incorporated in the likelihood as described in Sec. 3.1. The SM rate rescaled by the time-dependent asymmetries is now $\text{BR} (B_s \rightarrow \mu^+ \mu^-)_{\text{SM}} = (3.53 \pm 0.38) \times 10^{-9}$ [51], which is a value more appropriate for comparison with the experimental rate than the unscaled, $\sim 3.2 \times 10^{-9}$, one.

3. We have updated the nuisance parameters $M_t$ and $m_b(m_b)_{\overline{MS}}$ following [38]; see Table 2. The upgrade in $M_t$ has significant implications for $m_{h_1}$. The leading one-loop corrections to the Higgs mass squared are given by

$$\Delta m^2_{h_1} = \frac{3 m_t^4}{4 \pi^2 v^2} \left[ \ln \left( \frac{M^2_{\text{SUSY}}}{m^2_t} \right) + \frac{X^2_f}{M^2_{\text{SUSY}}} \left( 1 - \frac{X^2_f}{12 M^2_{\text{SUSY}}} \right) \right],$$

(16)

where $m_t$ is the running top quark mass\(^6\), $M_{\text{SUSY}}$ is the geometrical average of the physical stop

\(^5\)The best agreement between SOFTSUSY and NMSSMTools is obtained by setting the flag precision for the Higgs masses to zero which, therefore, was chosen as the default setting for our calculations.

\(^6\)Note that the running top quark mass is related to the pole mass through the formula given in Eq. (10) of
masses, \( M_{\text{SUSY}} \equiv \sqrt{m_{\tilde{t}_1} m_{\tilde{t}_2}} \), and \( X_t = A_t - \mu_{\text{eff}} \cot \beta \). Since \( \Delta m_{h}^2 \propto m_t^4 \) it is now easier to generate Higgs masses in agreement with the experimental values. In particular, as we highlighted in [30], a Higgs mass compatible with the observed excess at 126 GeV was rather difficult to achieve over the CMSSM parameter space. That tension has now become somewhat reduced, and we will show below that the correct Higgs mass can be obtained in the CMSSM limit of the CNMSSM.

4.1 Impact of the relic density

To set the ground for the presentation of our numerical results, we first comment on the role of the relic density of DM in selecting favored regions. The relic density is a strong constraint, since it is a positive measurement (in contrast to a limit) with a rather small experimental uncertainty (Table 1). On top of it, it is well known that in unified SUSY models with neutralino LSP the corresponding abundance \( \Omega_{\chi} h^2 \) is typically too large, or in other words, its annihilation in the early Universe is “generically” too inefficient, so that specific mechanisms for enhancing it are therefore needed. They, however, are only applicable in specific SUSY configurations. As a result, in most cases the regions of high probability in the global posterior will reflect one or more of the regions of parameter space where \( \Omega_{\chi} h^2 \) is close to the measured relic density of DM. The regions that are still allowed by direct SUSY searches are as follows:

1. The stau-coannihilation (SC) region [69]. As is known, in constrained SUSY models, like the C(N)MSSM, this is a narrow strip at a sharp angle to the \( m_{1/2} \) axis. The values of \( A_0 \) and \( \tan \beta \) are also constrained, as only for \(|A_0| < 2-3 \) TeV and \( \tan \beta \) not too large does the mass of the stau become light enough to be comparable with the neutralino mass, but not so light as to make it the LSP. Values of \( m_{1/2} \) that are excessively large, on the other hand, can suppress the annihilation cross section [70]. After other relevant constraints are included, the parameters of interest are, therefore, \( m_0 \lesssim 600 \) GeV, \( m_{1/2} \lesssim 1000 \) GeV, \(|A_0| \lesssim 3000 \) GeV and, when the neutralino is close to 100\% bino, \( \tan \beta < 30 \). A similar effect can also be obtained for large \( A_0 \) with the stop \( \tilde{t}_1 \) replacing \( \tilde{\tau}_1 \) [71].

2. The \( A \)-funnel (AF) region, where neutralinos annihilate through the resonance with the lightest pseudoscalar [72]. This mechanism can occur over broad ranges of the \((m_0, m_{1/2})\) plane where the pseudoscalar mass is close to twice the neutralino LSP mass, and is enhanced by large \( \tan \beta \) (\( \tan \beta \gtrsim 35 \)) and positive \( A_0 \).

3. The focus point/hyperbolic branch (FP/HB) region [73, 74], where the annihilation cross section can be enhanced by an increased higgsino component of the neutralino. For this to occur, \( \mu \) (or \( \mu_{\text{eff}} \) in the NMSSM) must be of the order of a few hundred GeV, and \( \tan \beta \) cannot be too large, \( \tan \beta \lesssim 45 \). In the \((m_0, m_{1/2})\) plane the condition corresponds to the region where \( m_0 \gg m_{1/2} \).

4.2 Impact of the Higgs mass

The measurement of the Higgs mass has added an important additional constraint on unified SUSY models. Below we will be discuss in turn the three cases listed earlier in Sec. 3.3.

Case 1. In Fig. 2(a) we show the marginalized posterior pdf in the \((m_0, m_{1/2})\) plane of the CNMSSM for case 1, obtained by imposing simultaneously all the constraints shown in Table 1. In these and the following plots the Bayesian 68\% (1\( \sigma \)) credible regions are indicated in dark blue and the 95\% (2\( \sigma \)) credible regions in light blue. Notice that the regions of high probability are located above the CMS razor limit, which we implemented in the likelihood as described in Sec. 3.2 and which is shown in the plots as a solid black line. In case 1 the role of the SM-like Higgs is played...
Figure 2: Marginalized 2D posterior pdf in (a) the \((m_0, m_{1/2})\) plane and (b) the \((A_0, \tan\beta)\) plane of the CNMSSM for case 1, constrained by the experiments listed in Table 1. The 68\% credible regions are shown in dark blue, and the 95\% credible regions in light blue. The solid black (dashed gray) line shows the CMS razor (ATLAS hadronic) 95\% C.L. exclusion bound.

by the lightest \(CP\)-even scalar (almost purely \(H_u^0\)-like), while \(h_2\) (almost purely \(H_d^0\)-like) and \(h_3\) (almost purely singletlike) are usually much heavier and decoupled. This case is thus expected to present features very similar to the CMSSM.

In Fig. 2(a) one can see two main 68\% credibility regions: the SC region on the lower left side, and the AF region on the top part of the plot. As is also the case in the CMSSM, besides giving the correct relic abundance, the SC region shows also the better fit to the Higgs mass, 
\[ m_{h_1} = 124.5 \text{ GeV} \]
This is because, as we explained in Ref. [30], in the SC region \(A_0\) can easily be negative without spoiling the relic abundance constraint. Large negative values of \(A_0\) are necessary to drive the parameter \(A_t\) to even larger negative values at the EW scale, thus making the stop mixing contribution to the loop corrections of the Higgs mass maximal. Note as well that the best-fit point is also located in the SC region.

In Fig. 2(b) we show the marginalized posterior in the \((A_0, \tan\beta)\) plane. The high probability “island” at negative \(A_0\) and \(\tan\beta \lesssim 25\) corresponds to the SC region.

In the CNMSSM the SC region appears to be more extended relative to the CMSSM [30], and somewhat larger Higgs masses also seem preferred, as we will show below. The increased relevance of the SC region is due to the fact that it is now much easier to obtain values of the Higgs mass closer to the correct one. This could be mistakenly thought to be a specific feature of the CNMSSM extended Higgs sector. We have checked that this is not the case: the Higgs mass is simply quite sensitive to the increased central value of the top mass, as we explained at the beginning of this section.

In Figs. 3(a) and 3(b) we show how the constraints affect the main observables responsible for
Figure 3: Marginalized 2D posterior pdf in (a) the \((m_{h_1}, m_{\tilde{t}_1})\) plane and (b) the \((m_{h_1}, X_t)\) plane, for the CNMSSM constrained by the experiments listed in Table 1 for case 1. The color code is the same as in Fig. 2.

the loop corrections to the Higgs boson mass. In Fig. 3(a) we show the posterior in the \((m_{h_1}, m_{\tilde{t}_1})\) plane. Notice that the lightest stop does not have to be excessively heavy in the SC region, \(m_{\tilde{t}_1} \simeq 1\) TeV, since large stop mixing compensates for smaller \(M_{\text{SUSY}}\). The correct Higgs mass is obtained since \(|X_t| \simeq 2.5\) TeV, as can be seen in Fig. 3(b) where we plot the posterior in the \((m_{h_1}, X_t)\) plane. On the other hand, one can see that in both figures the best-fit point lies outside of the 68\% credibility regions of the marginalized 2D pdf, when the latter is projected to the plane of these observables. This is a feature not uncommon in Bayesian analyses where the credibility regions map the “volume” of scan points satisfying well enough a certain set of constraints, rather than representing isocontours of the likelihood function, as is the case in frequentist analyses. The fact that the best-fit point is situated outside of the region of highest posterior probability for the considered observables simply tells us that, while for this point all the constraints are very well satisfied, it is also not very likely to obtain a similarly good value of the observable for similar choices of the input parameters. Particularly, in the case of Figs. 3(a) and 3(b) the majority of the points that satisfy all the constraints in the SC region present a Higgs mass in the range 120–123 GeV, while for the other regions it is even less.

Figure 2(a) also shows that the Higgs mass constraint favors the part of the AF region situated at \(m_{1/2} \gtrsim 1500\) GeV for a broad range of \(m_0\) values. Besides, in Fig. 2(b) one can see that in the \((A_0, \tan \beta)\) plane the AF region spans a large range of positive \(A_0\) values and \(\tan \beta\) is constrained to \(\tan \beta \gtrsim 40\). In this region one-loop corrections to the Higgs mass are driven up by a large stop mass \(m_{\tilde{t}_1} \sim 2–4\) TeV, as shown in Fig. 3(a), rather than large stop mixing which, given the preferred values of \(A_0\), is minimal (see Fig. 3(b)). Large values of \(M_{\text{SUSY}}\) push the Higgs mass close to the experimentally observed value, but not enough to reach it (for even larger \(M_{\text{SUSY}}, m_a_1\) becomes too heavy and resonant annihilation of neutralinos is not efficient). This can be interpreted as a sign
of some tension between the relic abundance and Higgs mass constraints in the AF region, which was investigated for the CMSSM in our previous paper [30]. The tension persists in the CNMSSM.

Only a limited fraction of the FP/HB region (which appears as a narrow 95%-credibility “tail” at $m_0 \gg m_{1/2}$) survives, as was the case for the CMSSM, despite the fact that the relic density is well satisfied over there. As we pointed out in [30], some tension with the 126 GeV Higgs boson mass arises not only in the AF but also in the FP/HB region where $\mu_{\text{eff}}$ is smaller than anywhere else. In fact, small values of $\mu_{\text{eff}}$ can be obtained only for relatively small values of $|A_t|$, as can be seen in Fig. 4(a), where we show the posterior in the weak scale parameters $A_t$ and $\mu_{\text{eff}}$ (notice that $A_t \approx X_t$ over all parameter space). For the chosen range of $m_0$, in the FP/HB region $M_{\text{SUSY}}$ cannot be very large either, so that the correct Higgs mass cannot be reached. The region of high posterior thus moves up towards larger $m_{1/2}$, where the neutralino has still a non-negligible higgsino component, but $M_{\text{SUSY}}$ is large enough to give the correct Higgs mass.

It is worth pointing out that $A_0 \simeq 0$ is not realized in the CNMSSM. This is because the lightest pseudoscalar $a_1$ becomes nonphysical for such values. The mass of $a_1$ is, for moderate and large values of $\tan \beta$, well approximated by $m_{a_1}^2 \approx -3\kappa s A_\kappa$ [12]. $A_\lambda$ and $A_\kappa$ are unified to $A_0$ at the GUT scale, and $A_\kappa$ barely runs, since the one-loop contribution to its $\beta$-function is negligible. As a consequence, in the CNMSSM $\kappa$ and $A_\kappa$ have always opposite signs and there are no points in the scan with $A_0 = 0$ or $\kappa = 0$.

We present in Fig. 4(b) the marginalized posterior pdf in the $(A_t, A_\tau)$ plane. The parameters show a clear linear correlation, which in the SC region (bottom left corner) results in large negative values for both observables, due to the fact that the correct Higgs boson mass requires large stop mixing, as discussed above.

Figure 5 shows the 2D posterior in the $(\lambda, \kappa)$ plane. One can notice the known correlation
between $\kappa$ and $\lambda$, in general $|\kappa|$ cannot exceed a given value of $\lambda$ by too much without causing a Landau pole in RGE running (see e.g. \cite{75} for details) and, on the other hand, $\lambda$ cannot exceed a given value of $|\kappa|$ by too much because the increased mixing between the doublet and singlet states lowers $m_{h_1}$ much below the observed value, where the likelihood becomes negligible, and eventually below the LEP bounds \cite{39}. In the SC region $\kappa$ is positive since $A_\kappa$ is negative, while in the AF and FP/HB regions these parameters switch signs. Hence, the upper branch shown in Fig. 5 corresponds to the SC region, and the lower one to both the AF and the FP/HB regions. Notice also that the upper branch is narrower than the lower one, due to the fact that SC occurs for limited ranges of the $m_0$ ($\lesssim 500$ GeV), $A_0$ (large and negative) and $\mu_{\text{eff}}$ ($\sim 1–2$ TeV) parameters. As a consequence, the condition for electroweak symmetry breaking requires $\kappa$ to be very close to $\lambda$ in the SC region.

At 95% credibility, the branches stretching along $|\kappa| \sim \lambda$ show an absolute upper bound in $\lambda$, which changes slightly for regions of parameter space characterized by different mechanisms to reduce the relic abundance. Specifically one can see that, on the one hand, $\lambda \lesssim 0.16$ for the upper branch. Again, for the ranges of parameters required by SC, a larger $\lambda$ lowers $m_{h_1}$ below the scale preferred by the likelihood function because of the increased singlet-doublet mixing \cite{17}. On the other hand, in the AF region (right-hand part of the lower branch) $\lambda$ cannot exceed 0.12 by too much as this would increase $m_{a_1}$, pushing it off the resonance with the lightest neutralino. In the FP region (left-hand part of the lower branch) the bound is on negative $\kappa$, and is due to the chosen ranges for $m_0$ ($m_0 \leq 4000$ GeV) and the fact that $\mu_{\text{eff}}$ tends to be small there, as shown in Fig. 4(a).

Simply, when $\kappa$ is significantly below $-0.1$, it becomes difficult to obtain electroweak symmetry breaking.

We want to reemphasize that, when the global constraints are considered, case 1 presents a very CMSSM-like character. The parameter $\lambda$ is small, and its effect on $m_{h_1}$ is insignificant, given that $\tan \beta \gtrsim 4$ over all of the regions of high posterior probability, as shown in Fig. 2(b). In the SC region the lightest Higgs mass can assume values close to 126 GeV more easily than what was
observed in our work on the CMSSM, but the reason lies in the updated value of the top mass used for the present analysis.

In Fig. 6(a) we show the marginalized posterior in the \((\tan \beta, m_{h_1})\) plane and in Fig. 6(b) the \((m_{a_1}, \tan \beta)\) plane. We also overlap a distribution of samples uniformly selected from our nested sampling chain. Notice that the density of samples reflects their relative posterior probability. One can see in Fig. 6(a) that, in the SC region (left island) the tension between the correct Higgs mass and the other constraints is much ameliorated. Figure 6(b) shows confirmation of the CMSSM-like nature of this case, as the pattern of high posterior mirrors the one found in Ref. [30].

**Case 2.** The NMSSM allows more freedom in the Higgs sector than the MSSM, due to the extended number of parameters. Even in its partially constrained version, there is a possibility of obtaining a light \(h_2\), which we found to be a mixture of \(H_u\) and \(S\) fields. A non-negligible singlet component creates the difference in the Higgs sector between this scenario and case 1. In the rest of this section we analyze the consistency of an \(h_2\) signal with the observed excess at the LHC.

In Fig. 7(a) we show the posterior pdf in the \((m_0, m_{1/2})\) plane for case 2. The favored parameter space is now drastically reduced with respect to case 1. Only the SC region, where the best-fit point is located, and the FP/HB region survive the requirement of having \(m_{h_2} \approx 126\) GeV.

In Fig. 7(b) we show the posterior pdf in the \((A_0, \tan \beta)\) plane. In both regions the range preferred for \(A_0\) does not extend much from zero, \(-400 \, \text{GeV} < A_0 < 400 \, \text{GeV}\). The reason is that \(|\kappa|\) is now limited to values less than 400 GeV by our requirement on the mass of \(h_2\). Specifically,\(^8\)

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\(^8\)Note that a gap around \(A_0 \approx 0\) in Fig. 7(b) comes from the physicality condition for \(a_1\), as discussed above.
Figure 7: Marginalized 2D posterior pdf in (a) the \((m_0, m_{1/2})\) plane and (b) the \((A_0, \tan\beta)\) plane of the CNMSSM constrained by the experiments listed in Table I for case 2. The color code is the same as in Fig. 2.

under the assumption of a moderate-to-large \(\tan\beta\) and as long as the parameters \(\mu_{\text{eff}}, \kappa_s\), and \(A_{(\kappa,\lambda)}\) do not exceed the EW scale by too much, a good approximation to the masses of the two lightest \(CP\)-even Higgs bosons at the tree level was found in [75]:

\[
m_{h_1,2}^2 \approx \frac{1}{2} \left\{ M_Z^2 + 4(\kappa s)^2 + \kappa_s A_\kappa \mp \sqrt{[M_Z^2 - 4(\kappa s)^2 - \kappa_s A_\kappa]^2 + 4\lambda^2 v^2 [2\lambda s - (A_\lambda + \kappa s) \sin 2\beta]^2} \right\}.
\]

In Eq. (17), the second term under the square root is suppressed with respect to the EW scale because \(\lambda\) is small, as we shall see below. One can see that in the regime where \(|\kappa|s < M_Z\), the mass of \(h_2\) is of order \(M_Z\) and \(m_{h_1}\) scales as \(|\kappa|s\). Thus, the physicality condition \(m_{h_1}^2 \geq 0\) translates into the approximate relation \(|A_\kappa| \lesssim 4|\kappa|s\). On the other hand, in the regions where \(|\kappa|s > M_Z\), \(m_{h_2} \sim \kappa s\) and \(m_{h_1} \sim M_Z\). Values of \(m_{h_2}\) much greater than 126 GeV are disfavored by the likelihood function, so that \(|\kappa|s\) presents an upper bound, which translates into an upper bound on \(|A_\kappa|\).

Since in most of the parameter space \(s\) is very large, and \(\lambda\) and \(\kappa\) are correlated, the scan also shows upper bounds for \(\lambda\) and \(\kappa\), in a fashion very similar to what is shown in Fig. 5 for case 1. For case 2, in the SC region \(\lambda\) is very small, \(\lambda \lesssim 0.01\), while in the FP/HB region it can assume slightly larger values, \(\lambda \lesssim 0.04\). Obviously, the upper bound on \(|\kappa|s\) does not depend on any particular position in the parameter space, but the bound on \(\kappa\) (or \(\lambda\)) does, and is affected particularly by \(\mu_{\text{eff}}\). In the SC region \(\mu_{\text{eff}} > 600\) GeV while in the FP/HB region \(\mu_{\text{eff}} \simeq 200\) GeV.

Given the strong constraint on \(|A_0|\) placed by the mass of \(h_2\), the only way of obtaining the relic density though coannihilation with the lightest stau is if the lightest neutralino is a nearly pure singlino and very light. This is exactly what is observed in the SC region and, as a consequence, in that region \(\lambda\) and \(\kappa\) are bounded to be much smaller than in case 1 (the neutralino mass matrix
Figure 8: (a) Marginalized 2D posterior pdf in the \((m_{h_1}, m_{h_2})\) plane of the CNMSSM constrained by the experiments listed in Table 1 for case 1. (b) Marginalized posterior pdf in the \((m_{h_1}, m_{h_2})\) plane of the CNMSSM for case 2. The color code is the same as in Fig. 2.

With the convention used in this paper can be found, e.g., in [31], \(A_0\) can only be negative, and \(\tan \beta\) assumes larger values (\(\tan \beta \sim 30 - 35\), favored also by other constraints, e.g. \(\delta (g-2)_\mu\)) than in the same region of case 1, or of the CMSSM. For smaller values of \(\tan \beta\), or a positive \(A_0\), the neutralino would be mostly bino and the lightest stau would be the LSP.

In Figs. 8(a) and 8(b) we show the 2D posterior in the \((m_{h_1}, m_{h_2})\) plane for case 1 and case 2, respectively. One can see that in case 1 \(m_{h_2} \gg m_{h_1}\), while in case 2 the 68\% credibility region shows a preference for \(90 \text{ GeV} \lesssim m_{h_1} \lesssim 115 \text{ GeV}\).

Since in case 2 \(m_{h_2} \simeq 126 \text{ GeV}\), \(m_{a_1}\) assumes values quite small in the favored regions, \(m_{a_1} < 500 \text{ GeV}\). While it might appear that such a case is excluded by the recent \(H \rightarrow \tau \tau\) searches at the LHC [76], we point out that the limit does not apply to this case, as the relevant couplings for \(a_1 \rightarrow \tau \tau\) and \(a_1 \rightarrow bb\) are suppressed by the pseudoscalar mixing angle \(\theta_p\), i.e., when \(|\cos \theta_p| < 1\) [77]. We have checked that \(|\cos \theta_p|\) is very close to zero over the regions of interest.

Case 3. Case 3 (two degenerate light Higgs bosons) is in fact a subset of case 2 when it comes to the preferred parameter space, which is uniquely determined by the requirement of \(m_{h_2} \simeq 126 \text{ GeV}\) as was explained above. The 2D posterior pdf’s for the input parameters are in this case almost indistinguishable from the ones showed in Figs. 7(a) and 7(b) and the best-fit point is again situated in the SC region. We therefore refrain from showing them explicitly. However, this case presents also some characteristic features:

• \(h_1\) is a mixture of \(H_d\) and \(H_u\), with a predominance of the latter, while \(h_2\) is mainly singletlike, with a small fraction of \(H_d\).

• Both \(\lambda\) and \(\kappa\) are now much more limited and very close to zero. The reason for this is simple: in order to have the two lightest \(CP\)-even Higgs bosons almost degenerated in mass, one needs to
minimize the difference $m_{h_2}^2 - m_{h_1}^2$ from Eq. (17). This yields negligible values for the parameter $\kappa$ and, consequently, also for $\lambda$. Clearly, as a consequence, the singlino nature of the LSP in the SC region is a feature confirmed for case 3.

### 4.3 Impact of the cross section rates

In Fig. 9(a) we show the 2D posterior pdf in the $(R_{h_1}(\gamma\gamma), R_{h_1}(ZZ))$ plane for case 1. As one can see, the Higgs boson in this case is SM-like. Actually, it is known [16] that the enhancement of the signal strength in the $\gamma\gamma$ decay channel observed by both CMS and ATLAS cannot be obtained for the values of $\lambda$ that are favored by the global scan. As a consequence, $R_{h_1}(\gamma\gamma)$ cannot be fitted perfectly in the CNMSSM. This discrepancy effectively adds two units of $\chi^2$ homogeneously over the preferred parameter space, but it does not alter the posterior distribution. For the same reason $R_{h_1}(ZZ)$ cannot be perfectly fitted either, though its contribution to the total $\chi^2$ is smaller than 0.5 units of $\chi^2$, making this observable equally ineffective in constraining the posterior.

In Fig. 9(b) we present the posterior distribution for case 2. Once again, $R_{h_2}(\gamma\gamma)$ can hardly become larger than 1 over the preferred parameter space. The 95% credible region lies far from the central value of the observed enhancement and, in fact, even covers values lower than in case 1. $R_{h_2}(ZZ)$ presents similar behavior, although the suppression of the reduced cross section is highly welcome for this observable, as it places the calculated value closer to the rate observed at CMS. Smaller than 1 signal rates indicate less of a SM-like character for $h_2$, which is caused by the suppression of the SM couplings induced by its increased singlet component.

The posterior distributions presented in Figs. 9(a) and 9(b) indicate that, in both case 1 and case 2 it is in general extremely difficult to obtain the signal enhancement in the $\gamma\gamma$ channel. The scan naturally tends to stay in the regions of parameter space favored by all constraints. It is
therefore no surprise that among the points scanned for case 1 only two presented a $\gamma\gamma$ rate in the range 1.2–2, thanks to the reduced coupling of the signal Higgs boson to the bottom quarks. Such points present $\chi^2$ contributions to the relic density of order several 10s, and the $\chi^2$ contribution to $\text{BR}(B_s \rightarrow \mu^+\mu^-)$ is of order 100. In case 2 we found a dozen such points, for which the contribution to the relic density is even worse.

In case 3 one could expect to obtain an enhancement of $R_{h_{\text{sig}}}(\gamma\gamma)$ by adding the individual rates for both almost degenerate light scalars. However, the posterior pdf in the $\left(R_{h_1+h_2}(\gamma\gamma), R_{h_1+h_2}(ZZ)\right)$ plane is remarkably similar to the one shown in Fig. 9(a) due to the large singlet component of $h_2$, and we refrain from showing it again over here. In fact, in case 3 we were not able to find a single point with the enhanced $\gamma\gamma$ rate. Since case 3 is a subset of case 2 in terms of the favored parameter space, and the rates in the $\gamma\gamma$ and $ZZ$ channel do not show interesting features, we will not consider it separately from the other cases any further.

4.4 Prospects for DM direct detection and $\text{BR}(B_s \rightarrow \mu^+\mu^-)$

In this subsection we will discuss the impact of limits from direct DM searches on the preferred parameter space of the CNMSSM. This kind of experiments are complementary to direct LHC SUSY searches, as they are capable of testing neutralino mass ranges beyond the current and future reach of the LHC, and therefore could add new pieces of information to the global picture.

At present the most stringent limit on the spin-independent cross section $\sigma_{p}^{\text{SI}}$ comes from XENON100 [78]. In supersymmetric models it can then be plotted as a function of the neutralino mass in the form of an exclusion limit in the $(m_\chi, \sigma_{p}^{\text{SI}})$ plane.

We want to point out that the theory uncertainties are very large (up to a factor of 10) and strongly affect the impact of the experimental limit on the parameter space [41]. It was shown that, when smearing out the XENON100 limit with a theoretical uncertainty of order 10 times the given value of $\sigma_{p}^{\text{SI}}$, the effect on the posterior is negligible for regions of the parameters that appear up to 1 order of magnitude above the experimental line. Moreover, the main source of error (the so-called $\Sigma_{\pi N}$ term) arises from different, and in fact incompatible, results following from different calculations based on different assumptions and methodologies. Therefore, in this study we decided not to include the upper bound on $\sigma_{p}^{\text{SI}}$ from XENON100 in the likelihood function, but below we will discuss its possible effects on the properties of the model.

In Fig. 10(a), we present the posterior pdf in the $(m_\chi, \sigma_{p}^{\text{SI}})$ plane for the case 1. The solid red line shows the most recent 90% C.L. upper exclusion limit by the XENON100 Collaboration. One can see that the two high posterior probability regions (from SC on the left and AF on the right) are located well below it. A small 95% credible region (corresponding to the FP/HB region with the lightest neutralino being a mixture of bino and higgsino) would probably be excluded by adding the XENON100 limit to the likelihood, even taking into account significant theoretical uncertainties. One can also notice that XENON1T, a future ton-size DM detector (projected sensitivity represented as the dashed gray line), will be in a position to test the 68% credible regions.

The conflict with the XENON100 limit in case 2 (and case 3, which presents similar features) is even stronger. In Fig. 10(b) we show the posterior in the $(m_\chi, \sigma_{p}^{\text{SI}})$ plane. The high probability region above the experimental line presents the features of the FP/HB region: $\mu_{\text{eff}} \simeq 200\text{ GeV}$, and the lightest neutralino is a mixture of bino and higgsino. As a consequence, the spin-independent neutralino-proton cross section is larger and in this case already in strong tension with the XENON100 bound.

Notice that the SC region is not shown in Fig. 10(b) since the neutralino is a nearly pure singlino there, so that $\sigma_{p}^{\text{SI}}$ is several orders of magnitude below the XENON100 bound (and below
Figure 10: Marginalized 2D posterior pdf in the \((m_\chi, \sigma_{SI}^p)\) plane of the CNMSSM constrained by the experiments listed in Table 1 in (a) case 1 and (b) case 2. The solid red line shows the 90% C.L. exclusion bound by XENON100 (not included in the likelihood), and the dashed gray line the projected sensitivity for XENON1T. The color code is the same as in Fig. 2.

the range shown in the figure). However, we would like to point out that in case 2 (and case 3) strong constraints on the full parameter space can be placed as a result of the interplay between the limits provided by two completely different experiments—that test different observables by means of different experimental techniques—namely LHCb and XENON100. This is illustrated in Figs. 11(a) and 11(b), where we show the posterior pdf in the \((BR(B_s \to \mu^+\mu^-), \sigma_{SI}^p)\) plane for case 1 and case 2, respectively. The solid blue horizontal line shows the minimum 90% C.L. upper bound on \(\sigma_{SI}^p\) by XENON100 (obtained at \(m_\chi \simeq 50\) GeV), and the dotted blue horizontal line the corresponding projected sensitivity for XENON1T. The pink vertical band encompasses the 1σ experimental uncertainty on the recent LHCb measurement of \(BR(B_s \to \mu^+\mu^-)\) [35]. Figure 11(b) shows that, for cases 2 and 3, in the SC region \(BR(B_s \to \mu^+\mu^-)\) is strongly enhanced, due to the large values assumed by \(\tan\beta\) there, and it could be excluded by the next updated results from LHCb.

4.5 Fine-tuning

In this subsection we will address the issue of fine-tuning. Note that we will not delve into it, nor will we discuss which values of fine-tuning are acceptable or not from the point of view of naturalness. Our aim here is to simply present an estimate of fine-tuning (provided as an output by NMSSMTools v3.2.1) for the preferred parameter space of the model, leaving aside the discussion of the viability of the model itself, which would be a matter of personal prejudices.

The mass of the Z boson (which determines the EW symmetry breaking scale) can be expressed in terms of the supersymmetric parameters through the minimization condition of the Higgs po-
The fine-tuning problem of the MSSM [79] amounts to the fact that the parameters $m_{H_u}, m_{H_d}$ and $\mu$ need to be simultaneously tuned to a high precision to reproduce the correct value of $M_Z$. In the NMSSM $\mu$ is replaced by $\mu_{\text{eff}}$. In the framework of the unified theory, at the GUT scale $m_{H_u} = m_{H_d} = m_0$. They are then evolved down to the EW scale by means of the RGEs. Therefore, the right-hand side of Eq. (18) depends on the parameters of the model at the GUT scale.

The measure of fine-tuning associated with the parameter $p_i$ of the model is defined as [80, 79]

$$\Delta_{p_i} = \left| \frac{\partial \log M_Z^2}{\partial \log p_i^2} \right|. \quad (19)$$

In the CNMSSM, $p_i = \{m_0, m_{1/2}, A_0, \lambda, \kappa\}$. We do not present the fine-tuning measure due to the top quark Yukawa coupling, following the approach adopted in [74], and quantifying the fine-tuning associated only with the supersymmetric parameters. We define the fine-tuning measure $\Delta$ for a given model point as the maximal contribution to fine-tuning among all the model’s parameters for that point,

$$\Delta = \text{Max}(\Delta_{p_i}). \quad (20)$$
In Figs. 12(a) and 12(b) we present the isocontours of the fine-tuning measure $\Delta$ in the $(m_0, m_{1/2})$ plane for cases 1 and 2, respectively. The isocontours reflect the value of $\Delta$ for the vast majority of the points included. They are superimposed on the 2D posterior distributions. Case 1 presents very CMSSM-like behaviour, where smaller fine-tuning can be achieved only in the FP/HB region due to the relatively low values of $\mu_{\text{eff}}$. Note that for the same reason $\Delta$ is larger in the SC region which is characterized by larger $\mu_{\text{eff}}$. On the other hand, case 2 is less fine-tuned ($\Delta < 50$ in a vast region of the parameter space preferred at $2\sigma$), which is a reflection of the fact that the parameter space is already highly constrained by the requirement of $m_{h_2} \approx 126$ GeV. In Figs. 13(a) and 13(b) we show for what percentage of the total number of allowed points each of the $p_i$’s yields maximal fine-tuning. For example, $\kappa$ gives maximal fine-tuning for 94% of the points in case 1,
while $A_0$ is the main contributor for the vast majority of the points in case 2.

### 4.6 Relaxing $(g-2)_\mu$ and the case of negative $\mu_{\text{eff}}$

In our recent study of the CMSSM [30] we considered the effect of relaxing the $\delta (g-2)_\mu$ constraint. The reason was based on the observation that the poor fit of the CMSSM was the result of basically that single constraint, which simply could not be reproduced after including especially direct superpartner mass limits from the LHC. This appears to be a general feature of all SUSY models where slepton and squark masses are assumed to be comparable, including simple unified models like the CMSSM or CNMSSM. We simply state it as a conclusion reached by many studies. While we do not feel to be in a position to comment on the reliability of theoretical calculations of the SM $(g-2)_\mu$ which are strongly affected by nonperturbative effects related to low-energy strong interactions, especially the hadronic light-by-light contribution (for more details see, e.g., the Introduction of [30] and references therein), we believe that it thus makes sense to consider global scans where the constraint is removed. We showed in [30] that for the CMSSM the better fit was obtained with $\mu < 0$ thanks to the constraints from $b$-physics, which present a much better $\chi^2$ for this choice of parameters.

Relaxing the $(g-2)_\mu$ constraint in the CNMSSM while keeping $\mu_{\text{eff}}$ positive has no apparent impact on the posterior distributions both for the parameters of the model as for the measured observables. Such behavior was to be expected for case 1, as it was already observed for the CMSSM in [30]. We checked that this is true also for case 2 and case 3, where relaxing the $(g-2)_\mu$ constraint while keeping $\mu_{\text{eff}}$ positive has little effect. Specifically, it reduces the statistical relevance of the SC region and slightly increases the size of the posterior in the FP/HB region where, as we discussed in Sec. 4.4, it is disfavored by the XENON100 bound.
Figure 15: Marginalized 2D posterior pdf in (a) the \((m_\chi, \sigmaSI_p)\) plane and (b) the \((\text{BR}(B_s\to \mu^+\mu^-), \sigmaSI_p)\) plane of the CNMSSM constrained by the experiments listed in Table 1, for case 1 without \((g-2)_\mu\) and with \(\mu_{\text{eff}} < 0\). The color code is the same as in Figs. 10 and 11.

We also confirm that, for case 1, the better overall fit is obtained with \(\mu_{\text{eff}} < 0\) for basically the same reasons as in the CMSSM. In Fig. 14(a) we show the 2D posterior pdf in the \((m_0, m_{1/2})\) plane for case 1, where we ignored the constraint from \(\delta (g-2)_\mu\) and set \(\text{sgn}(\mu_{\text{eff}}) = -1\). Differently from the CMSSM, where one could observe a clear predominance of the AF region, in the CNMSSM the SC, AF and FP/HB regions of parameter space now seem to be equally probable. This is not likely to be an intrinsic difference between the CMSSM and the CNMSSM; it is more probably due to the fact that the constraints are implemented with different numerical tools in the two models, as explained exhaustively at the beginning of Sec. 4. We note here that the global likelihood becomes flat over the regions of parameter space preferred by the relic density, and very little information can be extracted from the posterior.

In Fig. 14(b) we show the same posterior pdf in the \((A_0, \tan \beta)\) plane for case 1. As was the case for the CMSSM, one can see that the distribution of \(\tan \beta\) tends to favor slightly smaller values than in the positive \(\mu_{\text{eff}}\) case, particularly in the AF region.

In Fig. 15(a) we show the 2D posterior pdf in the \((m_\chi, \sigmaSI_p)\) plane for case 1. Since the posterior in the FP/HB region is much more extended with respect to the positive \(\mu_{\text{eff}}\) case, a large region of parameter space lies above the XENON100 bound, and has the potential of being tested with modest improvements in sensitivity. On the other hand, as was the case for the CMSSM, the AF region \((m_\chi > 400 \text{ GeV} \text{ and } \sigmaSI_p < 10^{-10} \text{ pb})\) is not likely to be further constrained by the new spin-independent cross section measurements planned for the next years, including XENON1T.

We shall analyze the \(\chi^2\) contributions from the individual constraints in the next subsection. Here we only repeat that, when the \((g-2)_\mu\) constraint is relaxed, the better \(\chi^2\) can be obtained for \(\mu_{\text{eff}} < 0\) thanks to the improved fit to \(\text{BR}(B_s\to \mu^+\mu^-)\) and \(\text{BR}(B\to X_s\gamma)\). To illustrate this feature we show in Fig. 15(b) the 2D posterior pdf in the \((\text{BR}(B_s\to \mu^+\mu^-), \sigmaSI_p)\) plane for case 1.
When $\mu_{\text{eff}} < 0$, a cancellation between the pseudoscalar and axial vector form factors takes place, with the result of improving the fit to $\text{BR} (B_s \to \mu^+\mu^-)$ over all of the parameter space, and particularly in the AF region, where the calculated values are pushed below the SM value.

For case 2 and case 3 it was not possible to perform the analysis of the effects of $\mu_{\text{eff}} < 0$, as the simultaneous interplay of different constraints strongly disfavors the entire parameter space of the model and no region of good fit appears. This can be understood by remembering that $m_{h_2} \approx 126 \text{ GeV}$ decisively favors small values of $|A_\kappa| \approx |A_0| \approx |A_\lambda|$ in the CNMSSM. On the other hand, physicality requires $m_{A_0}^2 > 0$, which for $\mu_{\text{eff}} < 0$ means $B_{\text{eff}} \equiv A_\lambda + \kappa s < 0$ [6], or $A_\lambda < -\kappa s$. Both constraints cannot be simultaneously satisfied for $A_0 < 0$ ($A_\kappa$, $A_\lambda$ and $\kappa$ negative) so that the scan tends to prefer small positive values of $A_0$. This generates a conflict with the relic density constraint: in the SC region $A_0 < 0$ is required for singlino LSP, whereas in the FP/HB region, when $\mu_{\text{eff}} < 0$ and $A_0 > 0$ the higgsino component of the neutralino is reduced and the relic

![Figure 16: SUSY mass spectra of the CNMSSM with $\mu_{\text{eff}} > 0$ for (a) case 1 and (b) case 2. (c) SUSY spectrum with $\mu_{\text{eff}} < 0$ and no $(g-2)_\mu$ in case 1. The narrow lines indicate the 95% credibility ranges and the thick bars the 68% credibility regions.](image)
Figure 17: Individual $\chi^2$ contributions to the best-fit points of the scans considered.

density becomes too large.

4.7 Mass spectrum and the best-fit points

In Figs. 16(a) and 16(b) we show the 1D marginalized posterior pdf’s for the SUSY mass spectrum in case 1 and case 2, respectively. The narrow lines indicate the 95% credibility regions, and the thick bars the 68% credibility regions.

Figure 16(a) shows the CMSSM-like character of case 1, since $h_3$, $a_2$ and $\chi_5$ are all heavy and effectively decoupled from the low scale spectrum. For case 2, Fig. 16(b) shows that requiring $m_{h_2} \simeq 126$ GeV forces the particles of the Higgs sector to be quite light, while the sfermions remain heavy, although they tend to be lighter than in case 1, since $m_{h_1}$ is lighter and it requires smaller loop corrections. The latter affect the scale of the stop and, through the assumption of unification, the other sfermions.

In Fig. 16(c) we show the mass spectrum for case 1 where we neglect $\delta (g - 2)_\mu$ and set $\mu_{\text{eff}} < 0$. Again we confirm the CMSSM-like nature.

In Fig. 17 we show the individual $\chi^2$ contributions of the applied constraints to the best-fit point, for the cases considered in this study. As could be expected, in case 1 the main contribution comes from $\delta (g - 2)_\mu$, once more confirming the CMSSM-like character of this scenario. In case 2 the contribution from $\delta (g - 2)_\mu$ is comparable to the one from BR ($B_s \to \mu^+ \mu^-$), due to the singlino character of the neutralino which favors higher $\tan \beta$, as explained in Sec. 4.4. When $\mu_{\text{eff}} > 0$, relaxing the $\delta (g - 2)_\mu$ constraint does not change significantly the contributions to $\chi^2_{\text{min}}$ due to the other constraints. This shows that the $\chi^2$ due to $(g - 2)_\mu$ is fairly homogeneous throughout the parameter space not yet excluded by direct LHC SUSY searches. However, for negative $\mu_{\text{eff}}$ the total $\chi^2$ improves by around 1–2 units, thanks to the improved fit to BR ($B \to X_s \gamma$), for which the contribution from the chargino-stop loop changes sign and tends to enhance the branching ratio, towards the experimental value [82]. As a consequence, the overall fit to the experimental
Table 3: CNMSSM input parameters, Higgs masses and fine-tuning measure for the best-fit points of our scans. Masses and $A_0$ are in GeV.

| Case, $\mu_{\text{eff}}$ | $m_0$ (GeV) | $m_{1/2}$ (GeV) | $A_0$ (GeV) | $\tan \beta$ | $\lambda$ | $m_{h_{\text{sig}}}$ (GeV) | $\Delta$ | $\chi^2_{\text{min}}$ |
|-------------------------|-------------|-----------------|-------------|-------------|---------|---------------------------|-------|---------------|
| With $(g-2)_{\mu}$     |             |                 |             |             |         |                           |       |               |
| Case 1, $\mu_{\text{eff}} > 0$ | 340.9      | 911.9           | -2546       | 12.0        | 0.017   | 124.5                     | 427   | 17.91         |
| Case 2, $\mu_{\text{eff}} > 0$ | 102.8      | 803.6           | -295.0      | 32.1        | 0.006   | 123.5                     | 396   | 18.45         |
| Case 3, $\mu_{\text{eff}} > 0$ | 124.7      | 958.8           | -356.7      | 33.7        | 0.001   | 120.3, 126.2              | 480   | 20.08         |
| No $(g-2)_{\mu}$        |             |                 |             |             |         |                           |       |               |
| Case 1, $\mu_{\text{eff}} < 0$ | 410.2      | 913.3           | -2764       | 14.8        | 0.017   | 123.9                     | 455   | 6.40          |

In Table 3 we show the parameters of the best-fit points obtained in our scans.

Table 3: CNMSSM input parameters, Higgs masses and fine-tuning measure for the best-fit points of our scans. Masses and $A_0$ are in GeV.

measurement improves.

One can finally notice that the contributions to $\chi^2_{\text{min}}$ due to $R_{h_{\text{sig}}}(\gamma\gamma)$ are sizeable in all three cases, as was explained in Sec. 4.3.

In Table 3 we show the parameters of the best-fit points obtained in our scans.

5 Summary and conclusions

In this paper we have presented the first global analysis of the CNMSSM which included the measurement of the mass and decay cross sections of the Higgs-like resonance observed at the LHC, the first evidence of nonzero BR ($B_s \to \mu^+\mu^-$) at LHCb, SUSY mass limits from direct searches, as well as the updated value of the top mass. We discussed in detail the possibility of either one of the lightest $CP$-even Higgs bosons of the model playing the role of the SM-like Higgs (case 1 and case 2 in the text) and that of the observed excess being due to a combination of two of them, both lying within the range $\sim 123$–129 GeV, after inclusion of a 3 GeV theoretical error on the Higgs mass calculation (case 3 in the text).

In contrast to the case with $m_S^2 = m_0^2$, explored for example in [83], we found that with our choice of parameters the CNMSSM allows for a SM-like $h_1$ as heavy as 125 GeV, especially in the stau-coannihilation region where the scan obtains a good compromise between the relic density and the $h_1$ mass constraint, owing to large negative $A_0$ values. The calculated value of $m_{h_1}$ is larger than what was previously found for the CMSSM [30] thanks to the increased value of the top pole mass. The overall fit is somewhat spoiled by the requirement of having $R_{h_1}(\gamma\gamma)$ consistent with the value reported by the CMS Collaboration, since it is virtually impossible, given our parameter choice and ranges, to obtain an enhancement in the cross section rate in case 1. A similar conclusion can be drawn for case 2 where, in turn, $h_2$ is required to have a mass around 126 GeV, which can also be achieved but at the cost of a poor fit to other observables. Case 3, with almost degenerate $h_1$ and $h_2$, was found not to be as interesting as anticipated, since the combined $R_{h_1+h_2}(\gamma\gamma)$ almost never exceeds 1, besides the fact that the high credibility posterior regions mimic those of case 2.

As mentioned in Sec. 2, we have adopted in this paper the choice $A_\kappa = A_0$ at the GUT scale. We checked with a few preliminary scans that this choice does not affect the shape and position of the posterior pdf’s in case 1. This make sense since, as we explained in Sec. 4, to satisfy all the constraints the model tends to its CMSSM limit, and the singlet field effectively decouples from the theory. Similarly, relaxing the unification condition on $A_\kappa$ would have little impact on the $(m_0, m_{1/2})$ 2D posterior in case 2 and case 3. In both cases the requirement of a very light $h_1$ constrains $m_0$ and $A_0$ substantially through $M_{\text{SUSY}}$ and the stop mixing parameter, independently of the value of $A_\kappa$ at the GUT scale. As a consequence, the relic density can only be satisfied in the regions of the $(m_0, m_{1/2})$ plane shown in Fig. 7(a). Some differences, on the other hand, can be
expected in the distribution of $\tan \beta$ in case 2 and case 3. Particularly, in the stau-coannihilation region, where the LSP is singlinolike, the region of high probability is likely to extend to values of $\tan \beta$ lower than the ones favored in this study. Consequently, the impact of the BR ($B_s \rightarrow \mu^+\mu^-$) constraint is likely to be reduced.

On the other hand, even by disunifying $A_\kappa$, we would not expect changes relative to our analysis of the di-boson Higgs decay rates. In a recent paper [10] it was shown that a $\gamma\gamma$ enhancement consistent with the observation is easily obtained in case 2. But we remind the reader that the study in question analyzed a model substantially less constrained than the one explored in here. In particular we have checked that, when allowing $\kappa$ and $\mu_{\text{eff}}$ to be free at the SUSY scale (as was done in [10]), the size of the favored parameter space in case 2 can increase significantly.

Finally, in this paper we also provided estimates of fine-tuning due to the various input parameters of the model in the form of isocontours in the $(m_0, m_{1/2})$ plane for cases 1 and 2. We noted that the maximum fine-tuning for most of the parameter space comes from two different sources in the two cases.

We assessed the effects of abandoning the $(g - 2)_\mu$ constraint since it cannot be reproduced in the CNMSSM, and more generally SUSY models with slepton-squark unification. In this case the overall fit actually improves considerably in case 1 for $\mu_{\text{eff}} < 0$, due to a better agreement of the model’s predictions for $b$-physics observables with experimental data, similarly to the CMSSM. Case 2 and case 3, on the other hand, are strongly disfavored for $\mu_{\text{eff}} < 0$ by the simultaneous impact of several constraints.

ACKNOWLEDGMENTS

S.M. would like to thank Cyril Hugonie for useful e-mail exchange regarding model implementation in NMSSMTools. L.R. thanks Gino Isidori and Matteo Palutan for helpful comments about BR ($B_s \rightarrow \mu^+\mu^-$).

This work has been funded in part by the Welcome Programme of the Foundation for Polish Science. K.K. is supported by the EU and MSHE Grant No. POIG.02.03.00-00-013/09. L.R. is also supported in part by the Polish National Science Centre Grant No. N202 167440, an STFC consortium grant of Lancaster, Manchester and Sheffield Universities and by the EC 6th Framework Programme MRTN-CT-2006-035505. The use of the CIS computer cluster at NCBJ is gratefully acknowledged.

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