Interstellar gas towards the TeV $\gamma$-ray sources HESS J1640–465 and HESS J1641–463

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ABSTRACT

We present a detailed analysis of the interstellar medium towards the tera electron volt (TeV) $\gamma$-ray sources HESS J1640–465 and HESS J1641–463 using results from the Mopra Southern Galactic Plane CO Survey and from a Mopra 7 mm-wavelength study. The $\gamma$-ray sources are positionally coincident with two supernova remnants (SNRs) G338.3–0.0 and G338.5+0.1, respectively. A bright complex of H ii regions connect the two SNRs and TeV objects. Observations in the CO(1–0) transition lines reveal substantial amounts of diffuse gas positionally coincident with the $\gamma$-ray sources at multiple velocities along the line of sight, while 7 mm observations in CS, SiO, HC$_3$N and CH$_3$OH transition lines reveal regions of dense, shocked gas. Archival H i data from the Southern Galactic Plane Survey was used to account for the diffuse atomic gas. Physical parameters of the gas towards the TeV sources were calculated from the data. We find that for a hadronic origin for the $\gamma$-ray emission, the cosmic ray enhancement rates are $\sim 10^3$ and $10^5$ times the local solar value for HESS J1640–465 and HESS J1641–463, respectively.

Key words: molecular data – supernovae: individual: SNR G338.3–0.0 – supernovae: individual: SNR G338.5+0.1 – ISM: clouds – cosmic rays – gamma-rays: ISM.

1 INTRODUCTION

HESS J1640–465 and HESS J1641–463 are two adjacent and intriguing very high energy (VHE, $E > 100$ GeV) $\gamma$-ray sources whose origins are uncertain. Knowledge of the distribution of interstellar gas towards these sources is vital in order to differentiate between possible models of theera electron volt (TeV) $\gamma$-ray production. In particular, understanding the hadronic production model of TeV $\gamma$-rays in which highly accelerated cosmic rays (CRs) interact with target atomic and molecular gas.

HESS J1640–465 is a VHE $\gamma$-ray source first discovered by the High Energy Stereoscopic System (HESS) during a survey of the Galactic plane (Aharonian et al. 2006). It is positionally coincident with the supernova remnant G338.3–0.0 (Whiteoak & Green 1996). Observations with XMM–Newton detected a slightly extended and asymmetric X-ray source towards the geometric centre of the supernova remnants (SNR) G338.3–0.0 (Funk et al. 2007). Follow-up observations with Chandra in X-rays revealed an extended nebula with a point-like source, a possible associated pulsar (Lemiere et al. 2009). It was suggested that the X-rays and VHE $\gamma$-rays were then due to synchrotron and inverse-Compton emission from a pulsar wind nebula (PWN). Multifrequency radio analysis by Castelletti et al. (2011) placed upper limits on the radio flux from the region of the supposed PWN. Observations with the Fermi Large Area Telescope (Fermi–LAT) revealed a high energy (HE) $\gamma$-ray source (1FGL 1640.8–4634) coincident with HESS J1640–465 (Slane et al. 2010).

Further observations by HESS (Abramowski et al. 2014a) show that the VHE $\gamma$-rays seen from HESS J1640–465 overlap significantly with the SNR shell of G338.3–0.0. The VHE $\gamma$-ray spectrum connects smoothly with the giga electron volt (GeV) $\gamma$-ray spectrum...
obtained by the analysis of 5 yr worth of Fermi-LAT data towards HESS J1640−465 (Lemoine-Goumard et al. 2014). The smooth, flat and featureless γ-ray spectrum strengthened the hadronic scenario in which CRs accelerated by the SNR are interacting with nearby gas (Abramowski et al. 2014a; Lemoine-Goumard et al. 2014). However, a contribution to the detected flux by a pulsar or PWN could not be ruled out. Recent work by Supan, Supanitsky & Castelletti (2016) looked at the spectral energy distribution (SED) of HESS J1640−465 using latest data from HESS and Fermi-LAT observations, together with an updated hadronic γ-ray model (Kafexhiu et al. 2014) and archival atomic (HI) and molecular data. Their fit yielded a spectra index Γ = 2.13 with a cut-off energy $E_{\text{cut}} = 54$ TeV. This hadronic model was found to fully describe the γ-ray spectrum of HESS J1640−465.

Shortly after the HESS publication (Abramowski et al. 2014a), Gotthelf et al. (2014) discovered pulsed X-ray emission using the Nuclear Spectroscopic Telescope Array emanating from the previously discovered X-ray source seen towards the centre of HESS J1640−465. The newly discovered pulsar PSR J1640−4631 has a period of 206 ms with a spin-down luminosity of $4.4 \times 10^{35}$ erg s$^{-1}$ and a characteristic age of 3350 yr. Modelling of leptonic γ-ray production suggested that a PWN could be responsible for the TeV emission from HESS J1640−465, although fine-tuning is required to explain the smooth GeV and TeV spectrum.

HESS J1641−463 was initially unnoticed by standard HESS detection techniques due to its low brightness and proximity to the bright source HESS J1640−465. Energy cuts and deeper observations led to the positive identification of the new TeV γ-ray source at a significance of $8.5\sigma$ at energies above 4 TeV (Abramowski et al. 2014b). HESS J1641−463 has an unusually hard spectrum (photon index $\Gamma \approx 2$) with no obvious sign of a cut-off. Analysis of Fermi-LAT data (Lemoine-Goumard et al. 2014) reported the detection of two distinct GeV sources positionally coincident with HESS J1641−463 and the nearby HESS J1640−465. HESS J1641−463 is positionally coincident with the radio SNR G338.5+0.1. The SNR itself is seen as a poorly defined circle of non-thermal emission (Whiteoak & Green 1996). The pair of SNRs seen towards the two HESS sources are connected by a complex of H II regions, which includes G338.4+0.0 and G338.45+0.06.

The production of TeV γ-ray emission from HESS J1641−463 via leptonic processes via a population of electrons with energies of several hundred TeV upscattering background photons was considered by Abramowski et al. (2014b). These electrons could be sourced from the coincident SNR G338.5+0.1 or even from a nearby PWN. This leptonic scenario, however, should be accompanied by a characteristic break in the γ-ray spectrum at multi-TeV energies resulting from the Klein–Nishina effect on the cross-section for inverse-Compton scattering at high energies. The lack of such a characteristic break in the γ-ray spectrum of HESS J1641−463 led the authors to disfavour the leptonic scenario.

A more promising scenario is that the γ-ray emission from HESS J1641−463 is due to interstellar medium (ISM) illuminated by highly accelerated CRs. Modelling by Abramowski et al. (2014b) indicate that the TeV spectrum of HESS J1641−463 could be produced by distribution of protons (with a power-law slope of $\sim 2.1$) interacting with molecular gas seen by using CO(1−0) data taken with the Nanten radio telescope. The proton spectrum would need to have a high cut-off energy (>100 TeV) and represents one of the hardest spectra associated with a TeV γ-ray source extending into the PeV energy range; a so-called PeVatron. The coincident SNR G338.5+0.1 could possibly be the source of these CR protons, provided it had a young age ($\lesssim 1$ kyr), as the proton spectrum agrees with predictions of diffusive shock acceleration in young SNRs. However, an older SNR (5−17 kyr; Abramowski et al. 2014b) would not be able to accelerate CRs to PeV energies (Bell et al. 2013), and would require another CR source. An intriguing idea is that VHE protons accelerated by the young SNR coincident with HESS J1640−465, SNR G338.3−0.0 (with an age of 1−2 to 5−8 kyr (Slane et al. 2010; Abramowski et al. 2014a) could be diffusively reaching the gas towards HESS J1641−463. The energy-dependent process of diffusion would preferentially allow higher energy CRs to reach the target material earlier (Aharonian & Atoyan 1996), producing the hard proton spectrum that is needed to generate the TeV γ-ray spectrum of HESS J1641−463.

Another puzzling aspect about HESS J1641−463 is the marked difference between the GeV and TeV components of its γ-ray spectrum. The GeV spectrum as measured by Fermi-LAT is very soft, which is in stark contrast to the very hard TeV spectrum as measured by HESS. This suggests that there may be two different sources to the GeV and TeV components. A possible scenario would be GeV γ-rays are produced by less energetic CRs from the old SNR G338.5+0.1 illuminating ambient gas, with TeV emission produced by higher energy CRs from the younger SNR G338.3−0.0.

Any attempt to fully understand the origin scenarios of both HESS J1640−465 and HESS J1641−463 requires a detailed understanding of the distribution of the ISM in the surrounding environment. Thus, we have used high-resolution data collected by the Mopra radio telescope in this study. As part of the Mopra Southern Galactic Plane CO Survey, the distribution of diffuse ($\tau \lesssim 10^3$ cm$^{-3}$) ISM was traced towards HESS J1640−465 and HESS J1641−463. In addition, we have taken complimentary data in the 7 mm wavelength band, targeting the dense ($\tau \gtrsim 10^5$ cm$^{-3}$) gas tracer CS(1−0) as well as the tracers SiO(1−0), CH$_3$OH and HCN.

In Section 2, we describe the parameters of the data taken by the Mopra radio telescope and the data reduction processes. The gas parameter calculations we apply to these data are described in Section 3. In Section 4, we investigate the gas distribution towards HESS J1640−465 and HESS J1641−463 and, in Section 5, we discuss the impact our results have on the possible emission scenarios for the TeV sources.

### 1.1 Distance to SNRs and H II complex

The distance to SNR G338.3−0.0 and SNR G338.5+0.1 and the H II complex containing G338.4+0.0 and G338.45+0.06 have previously been reported in several studies utilizing observations in the 21 cm H I spectral line.

Lemiere et al. (2009) derived a distance of 8−13 kpc for SNR G338.3−0.0 and the H II surrounding region based on H I absorption features. This is in agreement with previous work presented by Kothes & Dougherty (2007), who also used H I absorption to derive a distance of 11.7+2.6 −0.8 kpc for G338.4+0.0. The nearby SNR G338.5+0.1, coincident with HESS J1641−463, was found to have a very similar H I absorption profile as G338.4+0.0, which led to the assertion that it too was most likely located at $\sim 11$ kpc.

The velocity along the line of sight ($v_{LSR}$) of the H II regions in the complex have been measured to have values of $\sim$40 to $\sim$80 km s$^{-1}$ (Caswell & Haynes 1987; Russell 2003; Urquhart et al. 2012). The kinematic distance ambiguities towards these H II regions have been addressed and they have been constrained to the far distance (Urquhart et al. 2012).

This places the two SNRs and the H II complex in the Norma II spiral arm at the far side of the Galaxy. In our results in Section 4, we have used the Galactic rotation curve in Kothes & Dougherty...
(2007) to calculate distances for corresponding $v_{\text{LSR}}$. For purposes of our discussion in Section 5, we adopt a distance of 11 kpc for the two SNRs, H ii regions and both HESS J1640–465 and HESS J1641–463.

## 2 MOPRA OBSERVATIONS AND DATA REDUCTION

For the 7 mm targeted studies, initial Mopra observations towards HESS J1640–465 and HESS J1641–463 were taken in 2012 April. Four Mopra ‘On-the-fly’ (OTF) 20 arcmin $\times$ 20 arcmin area maps were taken resulting in a 40 arcmin $\times$ 40 arcmin region centred at $[l, b] = [338:26, -0:072]$. The scan length was 7.6 arcsec per cycle time of 2.0 s with spacings of 31.2 arcsec between each scan row. Each scan consisted of 79 cycles (~158 s). After every two scans, a sky reference position was observed for 18 cycles (~36 s) which was used for subtraction in the data reduction process. Three passes were observed towards each 20 arcmin $\times$ 20 arcmin region in alternating $l$ and $b$ scanning directions. This resulted in ~9 h of observations per 20 arcmin $\times$ 20 arcmin map. The 7 mm coverage is indicated by the large dashed black box in left-hand panel of Fig. 1.

In 2013 May, additional observations were taken in a smaller, 12 arcmin $\times$ 12 arcmin region centred at $[l, b] = [338:51, -0:083]$ towards HESS J1641–463. Similar scan parameters were used as in the 20 arcmin $\times$ 20 arcmin maps over six new passes resulting in ~3 times the observation time in this region. The additional observations resulted in greater sensitivity and a lower $T_{\text{RMS}}$ by a factor of ~1.7. This region is indicated by the dashed red box in the left-hand panel of Fig. 1.

The Mopra spectrometer, MOPS, was used to target specific molecular line tracers. MOPS is capable of recording in sixteen molecular transitions and spectral resolutions of the survey are 0.6 arcmin and 0.1 km s$^{-1}$, respectively. Full details about the observational parameters used in this survey can be found within the aforementioned papers.

### Table 1. The Mopra Spectrometer (MOPS) set-up for 7 mm observations.

| Molecular line | Frequency (GHz) | Detection | $T_{\text{RMS}}$ (K/Channel) |
|---------------|----------------|-----------|-----------------|
| $^{30}$SiO(J = 1–0, $v = 0$) | 42.373 365 | – | 0.04 |
| SiO(J = 1–0, $v = 3$) | 42.519 373 | – | 0.04 |
| SiO(J = 1–0, $v = 2$) | 42.820 582 | – | 0.04 |
| SiO(J = 1–0, $v = 0$) | 42.879 922 | – | 0.04 |
| SiO(J = 1–0, $v = 1$) | 43.122 079 | – | 0.04 |
| SiO(J = 1–0, $v = 0$) | 43.423 864 | Yes | 0.04 |
| CH$_3$OH | 44.069 476 | Yes | 0.04 |
| HCN(J = 40–39) | 45.119 064 | – | 0.04 |
| HCN(J = 17–16) | 45.264 750 | – | 0.04 |
| HCN(J = 5–4, F = 4–3) | 45.490 264 | Yes | 0.05 |
| $^{13}$CS(J = 1–0) | 46.247 580 | – | 0.05 |
| HCN(J = 16–17) | 47.927 275 | – | 0.05 |
| OCS(J = 4–3) | 48.206 946 | Yes | 0.06 |
| CS(J = 1–0) | 48.990 957 | Yes | 0.06 |

Notes. * Map $T_{\text{RMS}}$ values are for the smaller 12 arcmin $\times$ 12 arcmin region described in the text. This is where detections in all of the 7 mm lines were made except for CS(J = 1–0). For the detections in CS(J = 1–0) outside the 12 arcmin $\times$ 12 arcmin region, the $T_{\text{RMS}}$ value was ~0.1.

(49 GHz) and the velocity resolution of 7 mm zoom-mode data is ~0.2 km s$^{-1}$.

The CO(J = 1–0) line emission data are from the Mopra Southern Galactic Plane CO Survey (Burton et al. 2013; Braiding et al. 2015). This is a survey in the $^{12}$CO, $^{13}$CO and C$^{18}$O J = 1–0 lines over the $l = 305^{\circ}–345^{\circ}$, $b = \pm 0.5$ region of the Galaxy. The beam FWHM and spectral resolutions of the survey are 0.6 arcmin and 0.1 km s$^{-1}$, respectively. Full details about the observational parameters used in this survey can be found within the aforementioned papers.

OTF mapping data were reduced and analysed using ATNF analysis software, LIVEDATA, GRIDZILLA and MIRIAD, as well as custom IDL routines.

Figure 1. Left: Mopra $^{12}$CO(1–0) image [K km s$^{-1}$] integrated between $-53$ and $-23$ km s$^{-1}$ towards HESS 1641–463 and HESS 1640–465. Blue contours are HESS significance contours towards the TeV sources at the 5$\sigma$, 6$\sigma$, 7$\sigma$ and 8$\sigma$ levels at $E > 4$ TeV (Abramowski et al. 2014b). Dashed black and red boxes are the extent of the 7 mm observations and region of additional observations as discussed in text. Solid green circles are the positions of HESS J1640–463. The three dashed white circles are the regions from which CO spectra were extracted, as discussed in text. Right: solid black and blue lines are the average $^{12}$CO(1–0) and $^{13}$CO(1–0) emission spectra, respectively, within the rightmost and leftmost dashed white circles towards the TeV sources. $^{13}$CO scaled by factor of 2 for clarity. Velocity integration intervals used in Fig. 2 are numbered and indicated by the shaded boxes.
3 GAS PARAMETER CALCULATIONS (SPECTRAL LINE ANALYSIS)

To investigate the gas distribution towards HESS J1640−465 and HESS J1641−465, we calculated mass and density parameters using CO(1–0), CS(1–0) and H I data. Using the custom IDL routine \textsc{domcom}, we produced integrated intensity maps of the different molecular lines. The average column density of molecular hydrogen, $N_{\text{H}_2}$, was calculated from these maps following the corresponding methods outlined in the subsequent sections. The mass of gas in a region, $M$, is then estimated via the relation:

$$M = 2m_{\text{H}}N_{\text{H}_2}A,$$

where $A$ is the cross-sectional area of the region and $m_{\text{H}}$ is the mass of a hydrogen atom. From this, the average number density of the region $\bar{n}$ was estimated assuming that the thickness of the region (along the line of sight) had the same value as the height and width. Note that before the intensity values from the velocity-integrated maps could be used to find the column density, they first had to be scaled by a correction factor to account for the beam efficiencies of Mopra at different frequencies. The Mopra extended beam efficiency at 115 GHz (CO(1–0) lines) is $\eta_{\text{XB}} = 0.55$ (Ladd et al. 2005), while in the 7 mm band at 49 GHz (CS(1–0) lines), $\eta_{\text{XB}} = 0.56$ (Urquhart et al. 2010).

3.1 CO

In this work, to convert brightness temperature to column density, we have adopted the value of the CO(1–0) X-factor to be $X_{\text{CO(1–0)}} \sim 1.5 \times 10^{20}$ cm$^{-2}$ (K km s$^{-1}$)$^{-1}$ (Strong et al. 2004). This allows us to calculate the average $H_2$ column density in a region, $N_{\text{H}_2} = X_{\text{CO(1–0)}}W_{\text{CO(1–0)}}$, where $W_{\text{CO(1–0)}}$ is the measured $^{12}$CO(1–0) intensity.

The optical depth of the $^{12}$CO line, $\tau_{12}$, was calculated by comparing $^{12}$CO and $^{13}$CO line emission. Following Burton et al. (2013), in the limit where the $^{12}$CO line is optically thick and the $^{13}$CO line is optically thin, $\tau_{12}$ is given by

$$\tau_{12} = \frac{X_{12/13}}{R_{12/13}},$$

where $R_{12/13}$ is the ratio of the brightness temperature of the $^{12}$CO and $^{13}$CO lines and $X_{12/13} = [^{12}\text{C}/^{13}\text{C}]$ is the isotope abundance ratio. This abundance ratio was determined via $X_{12/13} = 5.5R + 24.2$, where $R$ is the galactocentric radius in kiloparsec (Henkel, Wilson & Bieging 1982).

3.2 CS

The CS($J = 1$) column density was calculated using equation (9) from Goldsmith & Langer (1999). This equation expresses the upper level column density in terms of the observed integrated line intensity. The optical depth term required in this equation was determined from the CS(1–0)–$^{34}$S(1–0) intensity ratio in regions where $^{34}$S(1–0) was detected. We adopted the elemental abundance of 22.5 for [CS]/[$^{34}$S] and calculate the optical depth following equation (1) of Zinchenko et al. (1994).

Assuming local thermodynamic equilibrium at $T_{\text{rot}} \sim 10$ K, the total column density of CS is a factor of $\sim 3.5$ times than of the CS($J = 1$) column density. This temperature assumption introduces a small systematic error into our CS(1–0) column density estimates. A factor of 0.7–1.2 error would be associated with a temperature variation between 5 and 15 K. We assume a molecular abundance of CS to molecular hydrogen to be $\sim 10^{-9}$ (Frerking et al. 1980).

3.3 H I

The Southern Galactic Plane Survey (SGPS; McClure-Griffiths et al. 2005) provided H I data towards HESS J1640−465 and HESS J1641−465. Strong absorption features due to continuum sources are seen in data corresponding to the H II regions G338.4+0.0, G338.45+0.06 and G338.39+0.16. Where H I emission features are present, we calculate the column density using an H I X-factor, $X_{\text{HI}} = 1.823 \times 10^{18}$ cm$^{-2}$ (K km s$^{-1}$)$^{-1}$ (Dickey & Lockman 1990).

4 RESULTS

Overall, the CO transitions reveal a distribution of gas along the line of sight towards the TeV sources. Significant detections made in CS(1–0) transitions reveal dense molecular cores within the gas distribution. We also note that detections were made in the SiO(1–0), CH$_2$OH (I) and HCN(N=4, F = 4–3) transitions towards the dense cores. We discuss these detections in more detail below.

4.1 CO(1–0) emission

$^{12}$CO and $^{13}$CO line emission data from the Mopra survey was studied towards HESS J1640−465 and HESS J1641−463. $^{12}$CO(1–0) is the standard tracer for diffuse molecular hydrogen gas, while the $^{13}$CO(1–0) line is generally optically thin with $^{13}$CO being approximately 50 times less abundant than $^{12}$CO. Detections in both isotopologues lines were made towards the TeV sources, as well as in other adjacent regions.

CO(1–0) emission towards HESS J1640−465 and HESS J1641−463

A substantial amount of CO(1–0) emission appears to be overlapping the line of sight towards HESS J1640−465 and HESS J1641−463. The left-hand panel in Fig. 1 is an integrated emission image of $^{12}$CO(1–0) data from the Mopra survey between $-53$ and $-23$ km s$^{-1}$ towards the two TeV sources. The right-hand panel of Fig. 1 displays the average $^{12}$CO(1–0) and $^{13}$CO(1–0) emission spectra of the regions corresponding to the reported intrinsic Gaussian size of HESS J1640−465 and the maximum Gaussian extent of HESS J1641−463 indicated in the left-hand panel by rightmost and leftmost white dashed circles, respectively. The central white dashed circle in the left-hand panel of Fig. 1 indicates the location of intense CO(1–0) emission seen towards a region that bridges HESS J1640−465 and HESS J1641−463 and is discussed further in a later part of this section.

Multiple broad emission components are seen in the CO(1–0) spectra towards HESS J1640−465 and HESS J1641−463 in the right-hand panel of Fig. 1 between $-140$ and 0 km s$^{-1}$. The velocity positions of these components are indicated by the shaded rectangles in the right-hand panel of Fig. 1 and are labelled as indicated.
Figure 2. Integrated $^{12}$CO(1–0) emission images [K km s$^{-1}$] over indicated velocity intervals. Single blue 5σ significance HESS contour used for clarity. The position and extent of SNR G338.5+0.1 and SNR G338.3-0.0 are indicated by the left and right solid green circles, respectively, in each panel.

Fig. 2 shows panels of the integrated $^{12}$CO(1–0) emission over said velocity intervals.

Components 1, 2 and 3 (red, yellow and orange shaded boxes) appear both towards HESS J1640–465 and HESS J1641–463 and are centred at $\sim$−30, −40 and −50 km s$^{-1}$, respectively. The gas traced in these components are the most likely candidates to be associated with the H$\pi$ complex, which includes G338.4+0.0 and G338.45+0.06 with $V_{\text{LSR}}$ $\sim$ −30 to −40 km s$^{-1}$. This motivates the integration range used in the left-hand panel of Fig. 1 which corresponds to the velocity space spanned by these three components.

In component 1 (−35 to −23 km s$^{-1}$), the $^{12}$CO(1–0) emission is very prominent in the spectrum towards HESS J1641–463. The corresponding integrated intensity image shows a molecular cloud positionally coincident with HESS J1641–463 that extends spatially to at least the Galactic-west and Galactic-north-western parts of SNR G338.3-0.0.

Gas is seen overlapping both TeV sources, as well as all around these sources, in the integrated image for component 2 (−45 to −35 km s$^{-1}$). Additionally, intense CO emission appears in the region between the TeV sources. An approximate ring of emission can be made out towards HESS J1641–463 and is discussed in a later section.

In the integrated image for component 3 (−53 to −45 km s$^{-1}$), the gas overlapping HESS J1640–465 appears to be connected to a cloud complex to the Galactic-west. Less gas appears to be directly overlapping HESS J1641–463 and the intense emission between the two TeV sources appears more towards the Galactic-south than in component 2.

The broad features in components 1, 2 and 3 in both $^{12}$CO and $^{13}$CO spectra appear to overlap each other. Thus, it is difficult to say with certainty if these are physically connected structures. As such, the mass and density parameters for these features were calculated individually. The spectrum in these components were fit with a multiGaussian function and the individual Gaussian functions were used to calculate mass and density parameters. The parameters of the fitted Gaussian functions and the calculated properties of the diffuse H$_2$ gas are displayed in Table 2.
Table 2. $^{12}$CO(1–0) line parameters, and the corresponding calculated gas parameters, from the apertures as indicated in Fig. 1. The line-of-sight velocity, $v_{\text{LSR}}$, linewidth (full width at half-maximum), $\Delta v_{\text{FWHM}}$, and peak intensity, $T_{\text{peak}}$, were found by fitting Gaussian functions to the $^{12}$CO(1–0) spectra. The optical depth was calculated by comparing the $^{12}$CO and $^{13}$CO line emission following Section 3.1. Masses and density have been scaled to account for an additional 20 per cent H$_2$ component.

| Component | Region       | $v_{\text{LSR}}$ (km s$^{-1}$) | Distance$^a$ (kpc) | $\Delta v_{\text{FWHM}}$ (km s$^{-1}$) | Peak (K) | Optical depth ($N_{\text{H}_2}$) (10$^{21}$ cm$^{-2}$) | Mass ($^b$) ($M_\odot \times 10^4$) | $\pi$ ($^b$) (10$^2$ cm$^{-3}$) |
|-----------|--------------|-------------------------------|--------------------|--------------------------------------|----------|------------------------------------------------|--------------------------------|------------------|
| 1         | HESS J1640–465 | $-31.6 \pm 1.1$               | 11.9               | $3.9 \pm 0.1$                        | 1.6 $\pm$ 0.1 | 10.5                                                      | 4.3                                               | 6.8              |
|           | HESS J1641–463 | $-29.0 \pm 0.1$               | 11.9               | $4.1 \pm 0.1$                        | 4.5 $\pm$ 0.1 | 11.7                                                      | 12.8                                                   | 9.7              |
|           | Bridge       | $-28.1 \pm 0.1$               | 11.9               | $5.2 \pm 0.1$                        | 3.5 $\pm$ 0.1 | 13.1                                                      | 12.5                                                   | 19.0             |
| 2         | HESS J1640–465 | $-40.7 \pm 0.1$               | 11.2               | $2.6 \pm 0.1$                        | 1.9 $\pm$ 0.1 | 8.5                                                        | 3.4                                                   | 4.7              |
|           | HESS J1641–463 | $-39.8 \pm 0.1$               | 11.2               | $2.7 \pm 0.1$                        | 2.5 $\pm$ 0.1 | 10.3                                                      | 4.6                                                   | 3.1              |
|           | Bridge       | $-40.5 \pm 0.1$               | 11.2               | $2.4 \pm 0.1$                        | 4.4 $\pm$ 0.1 | 11.1                                                      | 7.4                                                   | 9.9              |
| 3         | HESS J1640–465 | $-49.2 \pm 0.1$               | 10.8               | $4.2 \pm 0.1$                        | 2.4 $\pm$ 0.1 | 6.9                                                        | 6.9                                                   | 8.8              |
|           | HESS J1641–463 | $-47.0 \pm 0.2$               | 10.8               | $2.3 \pm 0.2$                        | 1.2 $\pm$ 0.1 | 11.1                                                      | 1.8                                                   | 1.1              |
|           | Bridge       | $-48.3 \pm 0.1$               | 10.8               | $4.2 \pm 0.1$                        | 3.9 $\pm$ 0.1 | 9.3                                                        | 11.0                                                  | 13.9             |

Notes. $^a$Assumed distances, $d_0$, used for mass and density calculations are derived from the Galactic rotation curve presented in Kothes & Dougherty (2007). However, these values are easily scaled for an arbitrary distance, $d$, by multiplying by $(d/d_0)^2$ and $(d/d_0)^{-3}$ for mass and density, respectively. $^b$The error in the calculated physical parameters are dominated by the statistical uncertainties associated with the CO to H$_2$ conversion factor $(X_{\text{CO}(1–0)})$ and is of the order of 30 per cent (Bolatto, Wolfire & Leroy 2013).

Emission in component 4 (−63 to −55 km s$^{-1}$) is seen only in the region towards HESS J1641–465. A small molecular cloud appears overlapping the Galactic-north upper half of TeV source.

Component 5 (−90 to −68 km s$^{-1}$) and component 6 (−92 to −81 km s$^{-1}$) both include emission in a long band of gas that passes through both TeV sources. Emission in component 6 has an additional tail end that extends to the Galactic-south-east of HESS J1640–465.

Component 7 (−103 to −90 km s$^{-1}$) has an arm-like structure of emission that overlaps through HESS J1641–463, while a minor amount of wispy gas is seen in component 8 (−108 to −97 km s$^{-1}$) in the Galactic-northern region of HESS J1640–465.

Component 9 (−125 to −108 km s$^{-1}$) includes features in the gas that overlap much of HESS J1640–465 and appears to be connected to a gas structure immediately to the Galactic-south.

As mentioned in Section 1.1, the H II complex and both SNRs have been established in literature to be at the far distance, with associated kinematic velocities of ~40 to ~30 km s$^{-1}$. This corresponds to a distance of ~11 to 12 kpc along the line of sight (using the rotation curve from Kothes & Dougherty 2007). The gas traced in components 1, 2 and 3 are the only candidates for association with the H II complex and SNRs from kinematic distance considerations, as the $v_{\text{LSR}}$ of other gas components along the line of sight will not yield a far distance solution of ~11–12 kpc.

It is possible that not all gas traced in components 1, 2 and 3 are located at the far distance, as contamination from molecular material located at the near solution may occur. However, the likely need for molecular gas to support the H II complex suggests that a significant fraction of the CO emission in components 1, 2 and 3 traces associated gas located at the far distance.

CO bubble feature seen at $v_{\text{LSR}}$ ~ −40 to −35 km s$^{-1}$

Fig. 3 shows the integrated $^{12}$CO(1–0) emission between −40 and −35 km s$^{-1}$. Overlaid are black contours indicating integrated $^{13}$CO(1–0) emission in the same velocity interval. Both data show an elliptic-like ring of emission seen approximately positionally coincident with HESS J1641–463. The location of this ring is indicated by the white dashed ellipse in the figure. The ellipse has semimajor and semiminor axis lengths of ~7 and 5 arcmin, respectively.
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Figure 4. Position–velocity image [K] (in Galactic longitude) of $^{12}$CO(1–0) emission towards the bubble feature seen towards HESS J1641–463 in the region indicated in Fig. 3. The approximate position of the cavity discussed in text is indicated by the dashed white ellipse. The solid white contours indicate CS(1–0) emission detected in our 7 mm observations. Note that the extent of the coverage in 7 mm only reaches the vertical green line in longitude.

From Fig. 3, the thickness of the ring is $\sim$3 arcmin. The kinematic distance along the line of sight is $\sim$11.4 kpc at $-40$ to $-35$ km s$^{-1}$. Under these assumptions, the column density of the gas enclosed by the ring is $N_{H_2} \sim 4 \times 10^{21}$ cm$^{-2}$, with a total mass of $\sim 8 \times 10^4$ M$\odot$. From Fig. 4, the expansion velocity of the bubble appears to be $\sim 5$–10 km s$^{-1}$. The expansion of the bubble would then have a kinetic energy of $\sim 2$–8 $\times 10^{49}$ erg.

If this were a wind-blown bubble, an O-type progenitor star with mass $\sim 27$ M$\odot$ would be able to create it, based on the bubble size of radius $\sim 25$ pc at a distance of $\sim 11.4$ kpc (Chen, Zhou & Chu 2013, and references therein). The energy required to produce such a bubble can then be calculated following the model presented by Chevalier (1999) and is $\sim 4 \times 10^{49}$ erg.

**CO(1–0) emission towards dense ‘bridge’ between HESS J1640–465 and HESS J1641–463**

In components 1, 2 and 3 of Fig. 2, we see an area of intense CO emission located towards the Galactic-south part of the region that bridges HESS J1640–465 and HESS J1641–463 which appears to span between $\sim 35$ and $-55$ km s$^{-1}$. This region is indicated by the central white dashed circle in Fig. 1. Fig. 5 shows the average $^{12}$CO(1–0) and $^{13}$CO(1–0) emission spectra in this region. Three components are seen in the $^{12}$CO spectra that match well with components 1, 2 and 3 in Fig. 1. Calculated mass and density parameters for these components are displayed in Table 2.

**CO(1–0) emission towards the Galactic-west of HESS J1640–465 and HESS J1641–463**

CO(1–0) emission over a very broad ($\sim 60$ km s$^{-1}$) velocity range can be seen in an extended molecular cloud structure to the Galactic-west of HESS J1640–465. The top panel of Fig. 6 displays an integrated image of the $^{12}$CO(1–0) emission between $-80$ and $-20$ km s$^{-1}$ over an extended region from $l$
4.2 7 mm line emission

In our 7 mm observations towards HESS J1640–465 and HESS J1641–463, detections were made in the CS(1–0), C\textsuperscript{34}S(1–\textsubscript{0}), SiO(J = 1–0, v = 0), HC\textsubscript{3}N(5–4, F = 4–3) and CH\textsubscript{3}OH (I) lines.

Dense gas in the region was traced by CS(1–0) and C\textsuperscript{34}S(1–\textsubscript{0}) emission. The CS(1–0) transition has a critical density for emission of \( \sim 10^5 \) cm\textsuperscript{-3} at a temperature of \( \sim 10 \) K, making it an ideal tracer for probing the deeper and denser inner regions of molecular clouds. SiO emission is usually produced behind shocks moving through molecular clouds (Gusdorf et al. 2008) from which the SiO(J = 1–0, v = 0) line can be detected. HC\textsubscript{3}N is often detected in warm molecular clouds and is associated with star forming regions, while the CH\textsubscript{3}OH (I) maser generally traces star formation outflows.

The location of the dense gas traced by the CS(1–0) line in our study are displayed via a velocity-of-peak-pixel map in Fig. 7. From the figure, we can see that most of strongest CS(1–0) emission occurs at a velocity consistent with components 1, 2 and 3 (\( \sim 53 \text{ to } -23 \text{ km s}^{-1} \)) in the CO(1–0) data. Several regions of significant CS(1–0) emission present themselves and are roughly grouped together as illustrated in Fig. 7. These groups are discussed below together with other detections made in the 7 mm band. The detections of the 7 mm lines aside from CS are shown in Fig. 8 overlaid on a Spitzer 8.0 \( \mu \)m image of the region.

7 mm emission in Group A

Group A is located slightly to the Galactic-north of HESS J1640–465 and HESS J1641–463 and is approximately coincident with a bright H II region G338.39+0.16. CS(1–0) emission in this region appears in the \( \sim -40 \text{ to } -30 \text{ km s}^{-1} \) velocity range. The morphology of the emission is extended in nature, forming a slight arc with what appears to be two dense clumps.

7 mm emission in Group B or ‘bridge’ region

Group B is the central bridge coincident with the H II complex between HESS J1640–465 and HESS J1641–463. A markedly strong amount of CS(1–0) emission is seen here spanning a broad
in an extended bridge of emission linking themselves as well as other smaller clumpy features. We note the good correlation between Bridge Core 1 and emission in $^{13}$CO(1−0) (indicated by the solid black contours in Fig. 9). Bridge Core 2, however, appears to be offset from the local maximum traced in $^{13}$CO.

Detections in the isotopologue transition C$^{18}$S(1−0), as well as in SiO(1−0) and HC$_3$N(−4, F = 4−3) were made towards core 1 and core 2. The left and centre panels of Fig. 10 displays the emission spectra in these lines towards Bridge Core 1 and Bridge Core 2. The spatial size of the cores was determined by fitting a Gaussian function to the line profile drawn through the centre of each core and the spectra extracted from circular apertures with sizes equal to the FWHMs (1.3 and 0.9 arcmin for Bridge Core 1 and 2, respectively). We note that all the 7 mm line emission peaks at the same velocity as the intense emission in CS(1−0); −40 and −32 km s$^{-1}$ for Bridge Core 1 and 2, respectively. Table 3 displays the 7 mm detection parameters and mass estimates calculated from the data in these cores. Mass parameters were calculated following Section 3.2 assuming the gas is at a distance of 11 kpc.

SiO(1−0) emission appears positionally coincident with Bridge Core 1 and Bridge Core 2 at the same velocity as that observed in CS(1−0). This suggests that both these cores have been disturbed by a shock passing through. A CH$_3$OH (I) maser is seen at the Galactic-north-east edge of Bridge Core 1, suggesting the presence of an outflow. Combined with the detection of HC$_3$N at the same position and velocity and that Bridge Core 1 and 2 appear to be embedded in the complex of H II regions, the shock is likely to be been caused by recent nearby star formation.

7 mm emission in Group C

Group C is a region towards the Galactic-eastern side of the gas structure located to the Galactic-west of HESS J1640−465 and HESS J1641−463 as traced in CO. Note that the extension of our 7 mm observations only reaches to include the region labelled ‘1’ in the top panel of Fig. 6. We see large-scale extended and broad emission in the region in CS(1−0). This emission is in the same kinematic velocity ranges as that of the CO(1−0) emission. In Fig. 6, the average spectra shown for Extended region 1 include the CS(1−0) emission spectrum in red. Emission is seen between $\sim$−80 and $\sim$30 km s$^{-1}$, similar to the profile seen in the $^{13}$CO and $^{12}$CO, and is likely tracing denser regions that exist inside cloud. There is also one dense core traced in CS which appears at $\sim$−120 km s$^{-1}$ (dark blue in Fig. 7).

7 mm emission in Group D

Emission in CS(1−0) is seen in the Group D region slightly overlapping the Galactic-east side of the HESS J1641−463 contours in the $\sim$−25 to $\sim$20 km s$^{-1}$ velocity range. It has a marginally extended morphology. The most intense emission, located towards the middle, is positionally coincident with a dense core detected in the NH$_3$(1−1) transition line by the H$_2$O Southern Galactic Plane Survey (HOPS; Purcell et al. 2012). A core of gas traced by CS emission is seen at $\sim$−80 km s$^{-1}$ (green in Fig. 7) within the Galactic-north-east bounds of HESS J1641−463. This $\sim$80 km s$^{-1}$ core appears marginally extended and is positionally coincident with detections made in NH$_3$ (1,1) in the HOPS survey. Detections in the isotopologue transition C$^{18}$S(1−0) were also made at this position, as well as in SiO(J = 1−0, v = 0) and HC$_3$N(5−4, F = 4−3). The average spectra of the 7 mm lines detected in an aperture centred at this core is

Figure 8. Spitzer 8.0 μm image towards HESS J1640−465 and HESS J1641−463. Single magenta contour is 5σ significance from HESS observations. Dashed black contours are integrated SiO(1−0) emission. Dashed black contours are integrated HC$_3$N(5−4, F = 4−3) emission. The velocities over which they are integrated are as labelled. White Xs indicate positions of observed CH$_3$OH (I) masers.

Figure 9. Position–velocity image [K] of CS in the region indicated by a solid green box in Fig. 7. Locations of Bridge Core 1 and Bridge Core 2 are labelled with arrows. Black contours are from Mopra $^{13}$CO(1−0) observations.

($\sim$20 km s$^{-1}$) velocity space. Group B is also roughly positionally coincident with the intense emission seen in the CO ‘bridge’ discussed earlier, with emission features at similar velocities.

Fig. 9 is a longitude– velocity image of CS(1−0) data in the region indicated by a solid green box in Fig. 7. From this image, there appears to be two separate dense cores with broad CS(1−0) emission in this region separated in velocity, but somewhat overlapping spatially along the line of sight. We label these Bridge Core 1 and Bridge Core 2 as illustrated. These cores appear to be embedded within a larger extended CS emission region C.
displayed in the right-hand panel of Fig. 10 and we note that the emission in each line peaks at \(-80\) km s\(^{-1}\). A CH\(_3\)OH (I) maser is also seen positionally coincident with this core at \(-79\) km s\(^{-1}\). The velocity at which this core is detected suggests that it is not associated with the H \(\pi\) complex (which has \(v_{\text{LSR}} \sim -30\) to \(-40\) km s\(^{-1}\)).

### 4.3 Hi emission

The atomic gas towards HESS J1640–465 and HESS J1641–463 was studied using H i data from the SGPS (McClure-Griffiths et al. 2005). Integrated velocity maps were generated from the H i emission cubes over the same velocity intervals as the components traced in CO. Images of the H i-integrated velocity maps can be found in the appendix Fig. A2. We note that a study of atomic gas using SGPS data towards HESS J1640–465 was carried out by Supan et al. (2016), which focused on the velocity ranges from \(-121\) to \(-111\) km s\(^{-1}\) and from \(-40\) to \(-25\) km s\(^{-1}\). We find that our results are similar to those presented towards HESS J1640–465.

There are prominent dips in the H i spectra towards the TeV sources which occur at velocities where emission features are seen in the CO spectra. These dips may be the result of H i self-absorption, caused by residual H i embedded in the CO. Fig. A3 in the appendix is an example of such a dip in the spectrum towards HESS J1641–463 in component 1 and the corresponding intense emission that is seen in CO. To reduce the effect that these self-absorption dips may have on the calculation of the atomic gas parameters and following the analysis technique in Fukui et al. (2012), we estimate the actual H i emission level by a linear interpolation connecting the adjacent shoulders of a dip. The dotted line in Fig. A3 demonstrates this interpolation. This is a conservative estimate as the true spectrum is likely peaked, rather than just a straight line.

From the corrected spectra and, following Section 3, mass and density estimates of the atomic gas contained in each component were calculated. Similar to the work by Supan et al. (2016), we find that when comparing the molecular gas traced by CO and the atomic gas traced by H i, the physical parameters of the atomic gas are a small fraction of molecular gas. The calculated masses of atomic gas in each component can be found in Table 4 in Section 5 and in Table A2 in the appendix.

### 5 DISCUSSION

As mentioned previously in Section 1, the production of \(\gamma\)-rays from the TeV sources HESS J1640–465 and HESS J1641–463 may be the result of hadronic scenarios, in which the accelerated CRs are interacting with ambient gas, or leptonic scenarios, in which energetic electrons upscatter background photons. We now consider
Table 4. Calculated cosmic ray enhancement values, \( k_{CR} \), for the intrinsic Gaussian size of HESS J1640–465 and the maximum Gaussian extent of HESS J1641–463 for the gas related to components 1, 2 and 3 as defined in Fig. 1. Molecular mass comes from CO analysis and atomic mass from \( H \perp \) analysis.

| Region                      | Velocity range (km s\(^{-1}\)) | Assumed distance (kpc) | Molecular mass (\( M_\odot \)) | Atomic mass (\( M_\odot \)) | Total mass (\( M_\odot \)) | \( k_{CR} \) \( ^a \) |
|-----------------------------|---------------------------------|------------------------|-------------------------------|-----------------------------|-----------------------------|---------------------|
| HESS J1640–465              | −35 to −23 (Component 1)       | 11.9                   | 68 000                        | 12 000                      | 80 000                      | 1000                |
|                            | −45 to −35 (Component 2)       | 11.2                   | 47 000                        | 9300                        | 56 000                      | 1400                |
|                            | −53 to −45 (Component 3)       | 10.8                   | 88 000                        | 7100                        | 95 000                      | 850                 |
|                            | −53 to −23 (Components 1, 2 and 3) | 11.0                  | 203 000                       | 28 000                      | 230 000                     | 350                 |
| HESS J1641–463              | −35 to −23 (Component 1)       | 11.9                   | 97 000                        | 5000                        | 102 000                     | 150                 |
|                            | −45 to −35 (Component 2)       | 11.2                   | 31 000                        | 3200                        | 34 000                      | 450                 |
|                            | −53 to −45 (Component 3)       | 10.8                   | 11 000                        | 2100                        | 13 000                      | 1200                |
|                            | −53 to −23 (Components 1, 2 and 3) | 11.0                  | 139 000                       | 10 000                      | 149 000                     | 100                 |

Notes. \(^a\)Note that the CR enhancement factor, \( k_{CR} \), is effectively independent of assumed distance as the distance terms in equation (3) cancel with the distance assumptions for the mass calculations.

5.1 Hadronic scenarios

The segment of emission that includes components 1, 2 and 3 in the CO spectra traces gas which is at a velocity within \( \sim 10–20 \) km s\(^{-1}\) of the reported systematic velocity of the \( H \perp \) regions in the \( H \perp \) complex (see Section 1.1). Assuming SNRs G338.3–0.0 and G338.5+0.1 and the TeV sources are all linked with this \( H \perp \) complex, the gas traced here is a potential target for accelerated CRs. The dense gas traced by CS at these velocities is found in a bridging region between the two TeV sources and may also be acting as CR-target material.

A relationship to calculate the flux of \( \gamma \)-rays above a given energy level produced by hadronic interactions between CRs and CR-target material from the mass of the target material was derived by Aharonian (1991). The expected \( \gamma \)-ray flux above some energy \( E_\gamma \), assuming an \( E^{-1.6} \) integral power-law spectrum, is given by

\[
F(\geq E_\gamma) = 2.85 \times 10^{-13} E_\gamma^{-1.6} \left( \frac{M_\odot}{d_{kpc}} \right) k_{CR} \ cm^{-2} s^{-1}, \tag{3}
\]

where \( M_\odot \) is the mass of the CR-target material in units of \( 10^4 \) \( M_\odot \), \( d_{kpc} \) is the distance in kiloparsec, \( k_{CR} \) is the CR enhancement factor above that observed at Earth and \( E_\gamma \) is the minimum energy of \( \gamma \)-rays in TeV.

From the results in Abramowski et al. (2014a), the \( \gamma \)-ray flux photon above 1 TeV towards HESS J1640–465 is determined to be \( F(>1 \) TeV) \( \sim 1.9 \times 10^{-12} \) cm\(^{-2}\) s\(^{-1}\). From Abramowski et al. (2014b), the flux above 1 TeV towards HESS J1641–463 is \( \sim 3.6 \times 10^{-13} \) cm\(^{-2}\) s\(^{-1}\).

The total amount of CR-target material towards HESS J1640–465 and HESS J1641–463 is taken to be the sum of the molecular and atomic mass traced by emission in CO(1–0) and \( H \perp \), respectively. These masses, together with the calculated CR enhancement factors \( k_{CR} \) for the total mass in components 1, 2 and 3, are displayed in Table 4. A complete list of \( k_{CR} \) values for every gas component along the line of sight can be found in Table A2 in the appendix. It should be noted that the \( k_{CR} \) values here refer to \( E \geq 1 \) TeV \( \gamma \)-rays and pertain only to higher energy CRs (\( \geq 10 \) TeV).

Thus, any CR energetics should be considered lower limits on the total CR energy. In addition, equation (3) assumes an \( E^{-1.6} \) integral power-law CR spectrum. This is different from the \( \sim E^{-1.1} \) CR integral spectra needed to fit the \( \gamma \)-ray spectra of HESS J1640–465 and HESS J1641–463 (Abramowski et al. 2014b; Supan et al. 2016). By scaling equation (3) appropriately, the calculated CR enhancement factors would reduce by \( \sim 40 \) per cent for HESS J1640–465 and HESS J1641–463.

A similar study was conducted by Supan et al. (2016) on the physical properties of the ISM towards HESS J1640–465 using the same SGPS \( H \perp \) data, but with archival CO data from Dame, Hartmann & Thaddeus (2001). The authors used different sized regions of integration and velocity ranges compared to those used here. Analyses utilizing the same region size and velocity ranges on Mopra CO survey data return mass and densities parameters consistent with those presented in Supan et al. (2016).

The CR enhancement factor \( k_{CR} \) above 1 TeV towards HESS J1640–465 for the gas traced in components 1, 2 and 3 are of the order of \( \sim 10^{3} \). This value is consistent with a nearby (within a few parsecs) and young SNR (\( \lesssim 5 \) kyr), such as G338.3–0.0 accelerating and injecting CRs into the ambient gas (Aharonian & Atoyan 1996). Thus, assuming the gas at either components 1, 2 or 3 are associated with the location of HESS J1640–465, a hadronic scenario is plausible. In a case where all of the gas traced in these components are summed and considered as CR-target material associated with HESS J1640–465, the required \( k_{CR} \) value becomes 350.

In the case of HESS J1641–463, the required \( k_{CR} \) value for the molecular cloud positionally coincident (component 1) is 150. Component 1 is dominant whereby summing the gas traced in components 2 and 3 marginally decreases the required \( k_{CR} \) value. If the molecular cloud in component 1 is indeed associated with HESS J1641–463, the hadronic scenario would be possible given its proximity with potential CR accelerators.

If the hadronic scenario holds true in both HESS J1640–465 and HESS J1641–463, then the total CR energy budget, \( W_{\gamma} \), can be given as \( W_{\gamma} = L_{\gamma} \tau_{pp} \), where \( L_{\gamma} \) is the luminosity in \( \gamma \)-rays. \( \tau_{pp} \) is the cooling time of protons through proton–proton collisions and is given by (Aharonian & Atoyan 1996): \( \tau_{pp} \approx 6 \times 10^{6} (n/1 \) cm\(^{-3})^{-1} \) yr, where \( n \) is the number density of the ambient gas.

HESS J1640–465 has a \( \gamma \)-ray luminosity of \( L_{\gamma} = 9 \times 10^{34} \) erg s\(^{-1}\) above 1 TeV at 11 kpc (Abramowski et al. 2014a), while HESS J1641–463 has a luminosity of \( 4 \times 10^{34} \) erg s\(^{-1}\) above 0.64 TeV at 11 kpc (Abramowski et al. 2014b). Thus, \( W_{\gamma} \sim 10^{39} (n/1 \) cm\(^{-3})^{-1} \) erg for HESS J1640–465, and \( W_{\gamma} \sim 10^{39} (n/1 \) cm\(^{-3})^{-1} \) erg for HESS J1641–463. The number densities for both TeV sources presented in Table 2 in components...
1, 2 and 3 are of the order of $\sim 10^2$ cm$^{-3}$. $W_{\nu}$ is then $\sim 10^{48}$ and
$\sim 10^{47}$ for HESS J1640–465 and HESS J1641–463, respectively, which is a fraction of the canonical amount of energy channelled into accelerated CRs by a SNR ($\sim 10^{50}$ erg).

We note here that the hadronic modelling of HESS J1640–465 done in Supan et al. (2016) used the parametrization of the $\gamma$-ray differential cross-section in the proton–proton interactions from Kafexhiu et al. (2014). Using ambient proton densities of $\sim 10^3$ cm$^{-3}$, they found the total energy in accelerated protons to be $\sim 10^{47}$–$10^{48}$ erg, consistent to first order with an SNR scenario.

In one of the scenarios discussed in Abramowski et al. (2014a) and Tang et al. (2015), CRs accelerated by the SNR G338.3–0.0, coincident with HESS J1640–465, have diffusively reached a molecular cloud coincident with HESS J1641–463. The centre of G338.3–0.0 lies $\sim 0.3$ from the far side of the maximum extent of HESS J1641–463, equivalent to $\sim 60$ pc at the assumed distance of 11 kpc. The maximum Gaussian extent of HESS J1641–463 is $0.05$ or $\sim 10$ pc at this distance. Thus, the filling factor of HESS J1641–463, assuming a spherical geometry with radius 10 pc, compared to the 60 pc radius sphere centred at SNR G338.3–0.0 is $\sim 0.005$. Assuming that $10^{49}$ erg was injected into accelerating CRs by G338.3–0.0 and assuming that the CRs are uniformly distributed within the sphere, the total amount of energy in CRs at HESS J1641–463 is $\sim 5 \times 10^{47}$ erg. This value is consistent with the value of $W_{\nu}$ calculated above for HESS J1641–463 and thus the presented origin scenario is energetically plausible for the observed ISM.

The separation from the Galactic-eastern edge of the SNR G338.3–0.0 to the position of HESS J1641–463 is $0.15$ or $30$ pc (at a distance of 11 kpc). The required CR enhancement factor of $k_{\text{CR}} \sim 100$ resulting from the diffusion of CRs from the SNR towards HESS J1641–463 is achievable according to Aharonian & Atoyan (1996). Fig. 1(b) of their paper shows the $k_{\text{CR}}$ values at several time epochs at a distance of 30 pc from an SNR. A $k_{\text{CR}}$ of $\sim 100$ is acquired at a source age between $10^4$ and $10^7$ yr, similar to the estimated age of SNR G338.3–0.0. Their calculations assumed a source spectral index of 2.2 and that $D_{10} = 10^{25}$ cm$^2$ s$^{-1}$, where $D_{10}$ is the diffusion coefficient when energy $= 10$ GeV. This value corresponds to slow diffusion and is not unexpected given the substantial amount of gas traced in the region between HESS J1640–465 and HESS J1641–463 in both CO and CS observations. This is because gas with larger values of $\pi$ will have greater magnetic fields. The corresponding increase in the interaction between CR particles and magnetic fields would increase the rate of scattering, thereby decreasing the diffusion coefficient.

We can estimate the diffusion coefficient through the gas in this bridge region using equation (2) from Gabici, Aharonian & Blasi (2007). The required value of the magnetic field inside the ISM is a function of $\pi$ and is calculated following Crutcher et al. (2010). In Section 4, we have calculated the values of $\pi$ for the diffuse and dense gas in the bridge region from CO and CS data respectively. These values have been presented in Tables 2 and 3. For the diffuse CO-traced gas, $B \sim 15$ µG and $D_{10} \sim \chi(4 \times 10^7)$ cm$^2$ s$^{-1}$. For the dense CS-traced cores, $B \sim 500$ µG and $D_{10} \sim \chi(7 \times 10^6)$ cm$^2$ s$^{-1}$. The parameter $\chi \leq 1$ is a suppression factor that accounts for the suppression of the diffusion coefficient inside a turbulent cloud. For a moderate value of $\chi \sim 0.1$, the diffusion coefficient in this region would agree with a slow diffusion scenario. This diffusion scenario is a theoretically plausible explanation for the $\gamma$-ray emission from HESS J1641–463. The hardness of the TeV emission would be explained by higher energy protons preferentially reaching CR target material earlier and the effective exclusion of low-energy CR due to the dense gas bridge.

As mentioned in Section 4.1, emission in CO(1–0) traces an extended molecular cloud structure to the Galactic-west of HESS J1640–465. The angular separation of this cloud is comparable to the separation between SNR G338.3–0.0 and HESS J1641–463 ($\sim 0.3$). If the scenario in which CRs escaping from SNR G338.3–0.0 are generating the TeV emission of HESS J1641–463 is true, then one might have expected this other giant molecular cloud to glow in $\gamma$-rays. However, while at similar angular separations from the SNR, this molecular cloud may be at different distance along the line of sight. The CO(1–0) and CS(1–0) emission (see Fig. 6) is very broad and is seen between $\sim 80$ and $\sim 20$ km s$^{-1}$ in velocity. This is in contrast with the emission from molecular cloud seen towards HESS J1641–463 which is seen at $\sim 30$ km s$^{-1}$. Differences between the Galactic-rotation curve solution at these velocities range up to several kiloparsecs. Since an increase in distance of even $\sim 100$ pc from the source SNR would drastically diminish the available CRs (Aharonian & Atoyan 1996), it is possible that CRs may not have yet reached this molecular cloud. In addition, CRs escaping from an accelerator can diffuse anisotropically, tending to propagate along magnetic field lines (e.g. Nava & Gabici 2013). It is possible that the orientation of the magnetic fields in this region are directing CRs away from this molecular cloud.

An alternate scenario is that SNR G338.5+0.1, coincident with HESS J1641–463, is accelerating CRs that are interacting with the ISM. Modelling by Abramowski et al. (2014b) indicate that the hard proton spectrum required to generate the $\gamma$-ray emission agrees well with CRs accelerated by a young SNR. The critical factor is then the age of SNR G338.5+0.1. A 5–17 kyr middle-aged SNR (Abramowski et al. 2014b) would disfavour this scenario and lend support to the diffusion scenario discussed above. In either case, the molecular cloud found in component 1 of our study towards HESS J1641–463 provides ample target material for accelerated CRs to interact with, producing $\gamma$-rays through the hadronic channel.

5.2 Leptonic scenarios

We now consider the leptonic scenarios, in which TeV emission is primarily due to accelerated electrons interacting with ambient photons via the inverse-Compton effect, for HESS J1640–465 and HESS J1641–463 in light of our ISM study.

The leptonic scenario for HESS J1640–465 has been developed and explored by several previous works (Funk et al. 2007; Lemiere et al. 2009; Slane et al. 2010; Abramowski et al. 2014a; Gotthelf et al. 2014). In particular, the scenario involves the electrons being accelerated at the termination shock of a PWN near the centroid of the TeVs source which is powered by PSR J1640–4631 (Gotthelf et al. 2014). In our ISM study and considerations in the previous section, we have shown that there is sufficient target material towards HESS J1640–465 for a purely hadronic origin, given a local CR accelerator such as SNR G338.3–0.0. As such, our study does not rule out either model and it possible that the TeV emission from HESS J1640–465 has contributions from both leptonic and hadronic processes, although some fine-tuning is required to explain the smooth power-law spectrum seen by Fermi–LAT (Lemoine-Goumard et al. 2014).
A leptonic origin has been previously considered for HESS J1641–463 (Abramowski et al. 2014b) but was strongly disfavoured, stemming from the lack of a characteristic break in the γ-ray spectrum and the extreme difficulty in accelerating a population of electrons to the required energies. For completeness, however, we now consider a leptonic diffusion scenario in which CR electrons, perhaps from the PSR J1640–4631, are diffusing through the gas bridge between HESS J1640–465 and HESS J1641–463.

The cooling time of CR electrons due to synchrotron radiation can be given by \( \tau_{\text{sync}} \approx (b_r \gamma)^{-1} \), where \( b_r = 1.29 \times 10^{-13} (B/mG)^2 \) s\(^{-1}\), and the diffusion time of CRs over a distance \( d \) is given by \( \tau_{\text{diff}} = d^2 / (6D(E)) \), where \( D(E) \) is the diffusion coefficient at energy \( E \) (Ginzburg & Syrovatskii 1964). We consider the case where \( E_\gamma = 5 \) TeV. At this energy, γ-rays produced via inverse-Compton scattering would have energies \( \sim 200 \) GeV (in the Thompson regime) which is near the lower limit of detectability by HESS.

Dense cores of gas within the bridge region are traced in CS observations with \( \pi \sim 10^5 \) cm\(^{-3}\). These cores have a diameter of \( \sim 2 \) arcmin, which corresponds to \( \sim 6 \) pc at a line-of-sight distance of \( 11 \) kpc. The magnetic field in these cores are calculated following Crutcher et al. (2010), using the values of \( \pi \) presented in Section 4. Using this, \( \tau_{\text{sync}} \) and \( \tau_{\text{diff}} \) were found to be \( \sim 10 \) yr and \( \sim 1 \) kyr, respectively. This implies that CR electrons would rapidly lose their energy via synchrotron losses and would be unable to pass through the dense cores. For completeness, we note that calculations using emission from the diffuse gas tracers \(^{12}\)CO and \(^{13}\)CO in these core regions give \( \pi \sim 4 \times 10^3 \) cm\(^{-3}\).

In an optimistic scenario, CR electrons could have paths that avoid the dense cores while diffusing through the gas bridge region. From Section 4, the diffuse gas traced by CO observations across the whole bridge region have \( \pi \sim 5 \times 10^2 \) cm\(^{-3}\). Assuming that the distance across the gas bridge is \( \sim 30 \) pc, \( \tau_{\text{sync}} \) and \( \tau_{\text{diff}} \) are calculated to be \( \sim 11 \) and \( \sim 4 \) kyr, respectively. Hence, in an optimistic scenario, some electrons would be able to diffuse through the gas bridge. However, realistically, this is somewhat unlikely given the prevalence of dense gas in the region, as traced by CS emission. CR electrons would be effectively blocked by the dense regions of the gas bridge and be unable to generate γ-rays which may be contributing to HESS J1641–463.

6 CONCLUSIONS

In this paper, we have used data collected by the Mopra Radio Telescope in the 3 and 7 mm wavelengths as well as archival H I data to investigate the molecular and atomic gas towards the VHE γ-ray sources HESS J1640–465 and HESS J1641–463. The gas investigated here may be target material for accelerated CRs, producing TeV γ-rays via hadronic interactions.

CO(1–0) observations from the Mopra Galactic Plane Survey revealed multiple diffuse molecular gas components at numerous velocities along the line-of-sight positionally coincident with both TeV sources. In particular, substantial detections were made at velocities within \( \sim 10–20 \) km s\(^{-1}\) of the reported systematic velocity of the H II region (\( \sim 32 \) km s\(^{-1}\)). The gas traced in Components 1, 2 and 3 as described in Section 4 (\( -53 \) to \( -23 \) km s\(^{-1}\)) may be then associated with the SNRs, H II region and the VHE γ-ray sources. Of particular note is the molecular cloud traced in Component 1 positionally coincident with HESS J1641–463.

7 mm observations in the CS(1–0) lines revealed a region of dense gas cores coincident with intense emission in the CO(1–0) lines. This gas formed a ‘bridge’ of material located between the two TeV γ-ray sources.

Mass and density estimates derived from CO, CS and H I for gas components towards HESS J1640–465 and HESS J1641–463 allowed for an investigation of the available CR target mass. Assuming that the total gas mass in Components 1, 2 or 3 towards HESS J1640–465 is CR-target material, then the required \( W_g \) is \( \sim 10^{19} \) erg and the required CR density would be of the order of \( \sim 10^2 \) times that seen at Earth. For HESS J1641–463, if the molecular cloud positionally coincident traced in Component 1 is CR-target material, then the required \( W_g \) is \( \sim 10^{20} \) erg and the required CR density would be of the order of \( \sim 10^3 \) times than seen at Earth.

We also investigated the scenario in which TeV emission from HESS J1641–463 is due to HE CRs from SNR G338.5+0.0, coincident with HESS J1640–465, diffusively reaching CR target material seen in our data. We find that the scenario is a plausible explanation which readily explains the hardness of the TeV emission from HESS J1641–463. We do not, however, discount the scenario in which SNR G338.5+0.1 coincident with HESS J1641–463 is providing the required CRs.

A scenario in which CR electrons from PSR J1640–4631 were diffusing towards HESS J1641–463 was considered. However, it is somewhat unlikely due to dense cores of gas present in the bridge between HESS J1640–465 and HESS J1641–463 which would effectively block the path of the electrons. This is in addition to arguments presented by Abramowski et al. (2014b) that disfavour a leptonic origin.

Future γ-ray measurements taken by next-generation ground-based γ-ray telescopes systems (e.g. Cherenkov Telescope Array) will have greatly increased sensitivity above 10 TeV and have angular resolutions similar to that in this study of the interstellar gas. This will allow more detailed morphological comparison between the TeV γ-ray emission and gas and allow a deeper investigation of the nature of HESS J1640–465 and HESS J1641–463.

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REFERENCES

Abramowski A. et al., 2014a, MNRAS, 439, 2828
Abramowski A. et al., 2014b, ApJ, 794, L1
Aharonian F. A., 1991, Ap&SS, 180, 305
Aharonian F. A., Atoyan A. M., 1996, A&A, 309, 917
Aharonian F., Akperjanian A. G., Bauer-Bachl A. R., Beilicke M., Benbow W., Berge D., 2006, ApJ, 636, 777
Bell A. R., Schure K. M., Reville B., Giacinti G., 2013, MNRAS, 431, 415
Bolatto A. D., Wolfire M., Leroy A. K., 2013, ARA&A, 51, 207
Braid C. et al., 2015, Publ. Astron. Soc. Aust., 32
Burton M. G. et al., 2013, Publ. Astron. Soc. Aust., 30, 44
Castelletti G., Giacani E., Dubner G., Joshi B. C., Rao A. P., Terrier R., 2011, A&A, 536, A98

MNRAS 464, 3757–3774 (2017)
Caswell J. L., Haynes R. F., 1987, A&A, 171, 261
Chen Y., Zhou P., Chu Y.-H., 2013, ApJ, 769, L16
Chevalier R. A., 1999, ApJ, 511, 798
Crutcher R. M., Wandel B., Heiles C., Fulgarone E., Troland T. H., 2010, ApJ, 725, 466
Dame T. M., Hartmann D., Thaddeus P., 2001, ApJ, 547, 792
Dickey J. M., Lockman F. J., 1990, ARA&A, 28, 215
Ferking M. A., Wilson R. W., Linke R. A., Wannier P. G., 1980, ApJ, 240, 65
Fukui Y. et al., 2012, ApJ, 746, 82
Funk S., Hinton J. A., Pühlhofer G., Aharonian F. A., Hofmann W., Reimer O., Wagner S., 2007, Astrophys. J., 662, 517
Gabici S., Aharonian F. A., Blasi P., 2007, Ap&SS, 309, 365
Ginzburg V. L., Syrovatskii S. I., 1964, The Origin of Cosmic Rays. Macmillan, New York
Goldsmith P. F., Langer W. D., 1999, ApJ, 517, 209
Gotthelf E. V. et al., 2014, ApJ, 788, 155
Gusdorf A., Cabrit S., Flower D. R., Pineau Des Forêts G., 2008, A&A, 482, 809
Henkel C., Wilson T. L., Bieging J., 1982, A&A, 109, 344
Irvine W. M., Goldsmith P. F., Hjalmarson A., 1987 Vol. 134 of Astrophysics and Space Science Library, Chemical abundances in molecular clouds. p. 561
Kafexhiu E., Aharonian F., Taylor A. M., Vila G. S., 2014, Phys. Rev. D, 90, 133014
Kothes R., Dougherty S. M., 2007, A&A, 468, 993
Ladd N., Purcell C., Wong T., Robertson S., 2005, Publ. Astron. Soc. Aust., 22, 62
Lemiere A., Slane P., Gaensler B. M., Murray S., 2009, ApJ, 706, 1269
Lemoine-Goumard M., Grondin M.-H., Acero F., Ballet J., Laffon H., Reposeur T., 2014, ApJ, 794, L16
McClure-Griffiths N. M., Dickey J. M., Gaensler B. M., Green A. J., Havercorn M., Strasser S., 2005, ApJS, 158, 178
Nava L., Gabici S., 2013, MNRAS, 429, 1643
Purcell C. R., Longmore S. N., Walsh A. J., Whiting M. T., Breen S. L., 2012, MNRAS, 426, 1972
Ruscell D., 2003, A&A, 397, 133
Simon R., Jackson J. M., Clemens D. P., Bania T. M., Heyer M. H., 2001, ApJ, 551, 747
Slane P., Castro D., Funk S., Uchiyama Y., Lemiere A., Gelfand J. D., Lemoine-Goumard M., 2010, ApJ, 720, 266
Strong A. W., Moskalenko I. V., Reimer O., Digel S., Diehl R., 2004, A&A, 422, L47
Supan L., Supanitsky A. D., Castelletti G., 2016, A&A, 589, A51
Tang Y., Yang C., Zhang L., Wang J., 2015, ApJ, 812, 32
Urquhart J. S. et al., 2010, Publ. Astron. Soc. Aust., 27, 321
Urquhart J. S. et al., 2012, MNRAS, 420, 1656
Whiteoak J. B. Z., Green A. J., 1996, A&AS, 118, 329
Zinchenko I., Forststroem V., Lapinov A., Mattila K., 1994, A&A, 288, 601
Figure A1. Integrated $^{13}\text{CO}(1-0)$ emission images (K km s$^{-1}$) over indicated velocity intervals. Single blue 5$\sigma$ significance HESS contour used for clarity and illustration purposes. The position and extent of SNR G338.5+0.1 and SNR G338.3-0.0 are indicated by the left and right solid green circles, respectively, in each panel.
Figure A2. Integrated H\textsc{i} emission images [K km s\textsuperscript{-1}] from SGPS data over indicated velocity intervals. Single white 5σ significance HESS contour used for clarity and illustration purposes. The position and extent of SNR G338.5+0.1 and SNR G338.3-0.0 are indicated by the left and right solid black circles, respectively, in each panel.
Figure A3. Average $\text{H}_\text{I}$ and $^{12}\text{CO}(1–0)$ emission spectrum towards HESS J1641–463 from the SGPS and Mopra CO survey, respectively. A possible example of a self-absorption dip in the $\text{H}_\text{I}$ is seen at $\sim-30$ km s$^{-1}$ in component 1, where a corresponding peak exists in the CO. The dashed line is the linear interpolation used to estimate the true $\text{H}_\text{I}$ emission.

Table A1. $^{13}\text{CO}(1–0)$ line parameters, and the corresponding calculated gas parameters, from the apertures as indicated in Fig. 1. Calculations were made following Section 3.1, but using the $^{13}\text{CO}(1–0)$ X-factor, $X_{^{13}\text{CO}(1–0)} = 4.92 \times 10^{20}$ (K km s$^{-1}$)$^{-1}$ (Simon et al. 2001). Masses and density have been scaled to account for an additional 20 per cent He component.

| Velocity range (km s$^{-1}$) | Region          | Distance$^a$ (kpc) | $\overline{N}_\text{H}_2$ $^b$ (10$^{21}$ cm$^{-2}$) | Mass$^b$ (M$_\odot$ $\times$ 10$^4$) | $\pi^b$ (10$^2$ cm$^{-3}$) |
|-----------------------------|-----------------|-------------------|-------------------------------|-----------------|-----------------|
| −35 to −23                  | HESS J1640–465  | 11.9              | 1.7                           | 2.7             | 0.8             |
| (Component 1)               | HESS J1641–463  | 11.9              | 6.7                           | 5.1             | 4.4             |
| Bridge                      |                 | 11.9              | 7.1                           | 10.1            | 3.3             |
| −45 to −35                  | HESS J1640–465  | 11.2              | 2.9                           | 4.3             | 1.4             |
| (Component 2)               | HESS J1641–463  | 11.2              | 3.0                           | 2.0             | 2.1             |
| Bridge                      |                 | 11.2              | 8.7                           | 11.7            | 4.3             |
| −53 to −45                  | HESS J1640–465  | 10.8              | 1.9                           | 2.5             | 0.9             |
| (Component 3)               | HESS J1641–463  | 10.8              | 0.6                           | 0.4             | 0.4             |
| Bridge                      |                 | 10.8              | 3.9                           | 4.9             | 2.0             |

Notes. $^a$Assumed distances, $d_0$, used for mass and density calculations are derived from the Galactic rotation curve presented in Kothes & Dougherty (2007). However, these values are easily scaled for an arbitrary distance, $d$, by multiplying by $(d/d_0)^2$ and $(d/d_0)^{-1}$ for mass and density, respectively. $^b$The error in the calculated physical parameters are dominated by the statistical uncertainties associated with the $^{13}\text{CO}$ to $\text{H}_2$ conversion factor ($X_{^{13}\text{CO}(1–0)}$) and is of the order of 30 per cent.
Table A2. Calculated CR enhancement values, $k_{CR}$, for the intrinsic Gaussian size of HESS J1640$-$465 and the maximum Gaussian extent of HESS J1641$-$463 for the gas related to all individual components as defined in Fig. 1. Molecular mass comes from CO analysis and atomic mass from H I analysis.

| Region       | $v_{LSR}$ range (km s$^{-1}$) | Assumed distance $^a$ (kpc) | Molecular mass (M$_{\odot}$) | Atomic mass (M$_{\odot}$) | Total mass (M$_{\odot}$) | $k_{CR}$ $^b$ |
|--------------|-------------------------------|-----------------------------|-------------------------------|---------------------------|--------------------------|--------------|
| HESS J1640$-$465 | -35 to -23 (Component 1) | 11.9 | 68 000 | 12 000 | 80 000 | 1000 |
|              | -45 to -35 (Component 2)  | 11.2 | 47 000 | 9300  | 56 000 | 1400 |
|              | -53 to -45 (Component 3)  | 10.8 | 88 000 | 7100  | 95 000 | 850  |
|              | -63 to -55 (Component 4)  | 10.4 | 15 000 | 4400  | 19 000 | 3800 |
|              | -90 to -68 (Component 5)  | 9.6  | 58 000 | 8000  | 64 000 | 950  |
|              | -92 to -81 (Component 6)  | 9.3  | 39 000 | 4200  | 43 000 | 1300 |
|              | -103 to -90 (Component 7) | 8.9  | 20 000 | 4300  | 24 000 | 2210 |
|              | -108 to -97 (Component 8) | 8.7  | 15 000 | 3000  | 18 000 | 2800 |
|              | -125 to -108 (Component 9) | 8.15 | 40 000 | 4700  | 45 000 | 990  |
| HESS J1641$-$463 | -35 to -23 (Component 1) | 11.9 | 97 000 | 5000  | 102 000 | 150 |
|              | -45 to -35 (Component 2)  | 11.2 | 31 000 | 3200  | 34 000 | 450  |
|              | -53 to -45 (Component 3)  | 10.8 | 11 000 | 2100  | 13 000 | 1200 |
|              | -63 to -55 (Component 4)  | 10.4 | 17 000 | 1000  | 18 000 | 750  |
|              | -90 to -68 (Component 5)  | 9.6  | 37 000 | 1700  | 39 000 | 300  |
|              | -92 to -81 (Component 6)  | 9.3  | 15 000 | 1100  | 16 000 | 680  |
|              | -103 to -90 (Component 7) | 8.9  | 13 000 | 1400  | 14 000 | 720  |
|              | -108 to -97 (Component 8) | 8.7  | 5500  | 1200  | 7000  | 1400 |
|              | -125 to -108 (Component 9) | 8.15 | 7100  | 1300  | 8000  | 1000 |

Notes. $^a$The assumed distance was calculated using the average $v_{LSR}$ in the interval with the Galactic rotation curve presented by Kothes & Dougherty (2007). For consistency, we have used the far distance solutions for every component. Masses can be scaled for an arbitrary distance, $d$, by multiplying by $(d/d_0)^2$ where $d_0$ is the assumed distance.

$^b$The CR enhancement factor, $k_{CR}$, was calculated following equation (10) from Aharonian (1991) considering the total masses presented in this table as CR-target material. Note also that $k_{CR}$ is independent of assumed distance as the distance terms in the equation cancel with the distance assumptions for the mass calculations.