Closing up a light stop window in natural SUSY at LHC

Archil Kobakhidze\textsuperscript{1}, Ning Liu\textsuperscript{2}, Lei Wu\textsuperscript{2}, Jin Min Yang\textsuperscript{3,4}, and Mengchao Zhang\textsuperscript{4}

\textsuperscript{1} ARC Centre of Excellence for Particle Physics at the Terascale, School of Physics, The University of Sydney, NSW 2006, Australia
\textsuperscript{2} Institution of Theoretical Physics, Henan Normal University, Xinxiang 453007, China
\textsuperscript{3} Department of Physics, Tohoku University, Sendai 980-8578, Japan
\textsuperscript{4} Institute of Theoretical Physics, Academia Sinica, Beijing 100190, China

(Dated: December 23, 2016)

Abstract

Top squark (stop) plays a key role in the radiative stability of the Higgs boson mass in supersymmetry (SUSY). In this work, we use the LHC Run-1 data to determine the lower mass limit of the right-handed stop in a natural SUSY scenario, where the higgsinos $\tilde{\chi}_1^0, \tilde{\chi}_2^0$ and $\tilde{\chi}_1^\pm$ are light and nearly degenerate. We find that the stop mass has been excluded up to 430 GeV for $m_{\tilde{\chi}_1^0} \lesssim 250$ GeV and to 540 GeV for $m_{\tilde{\chi}_1^0} \simeq 100$ GeV by the Run-1 SUSY searches for $2b + E_T^{\text{miss}}$ and $1\ell + \text{jets} + E_T^{\text{miss}}$, respectively. In a small strip of parameter space with $m_{\tilde{\chi}_1^0} \gtrsim 190$ GeV, the stop mass can still be as light as 210 GeV and compatible with the Higgs mass measurement and the monojet bound. The 14 TeV LHC with a luminosity of 20 fb$^{-1}$ can further cover such a light stop window by monojet and $2b + E_T^{\text{miss}}$ searches and push the lower bound of the stop mass to 710 GeV. We also explore the potential to use the Higgs golden ratio, $D_{\gamma\gamma} = \sigma(pp \to h \to \gamma\gamma)/\sigma(pp \to h \to ZZ^* \to 4\ell^\pm)$, as a complementary probe for the light and compressed stop. If this golden ratio can be measured at percent level at the high luminosity LHC (HL-LHC) or future $e^+e^-$ colliders, the light stop can be excluded for most of the currently allowed parameter region.

PACS numbers: 12.60.Jv, 14.80.Ly
I. INTRODUCTION

Weak scale supersymmetry is a leading candidate for solving the naturalness problem of the Standard Model, i.e. explaining the radiative stability of the hierarchy between the electroweak scale and high energy scales, such as Planck mass. In the minimal supersymmetric standard model (MSSM), the minimization condition of the Higgs potential is given by [1]

\[ \frac{M_Z^2}{2} = \frac{(m^2_{H_d} + \Sigma_d) - (m^2_{H_u} + \Sigma_u) \tan^2 \beta \tan^2 \beta - 1}{\tan^2 \beta - 1} - \mu^2, \]  

(1)

where \( m^2_{H_d} \) and \( m^2_{H_u} \) denote the weak scale soft SUSY breaking masses of the Higgs fields, \( \tan \beta = v_u/v_d \) and \( \mu \) is the higgsino mass parameter. \( \Sigma_u \) and \( \Sigma_d \) arise from the radiative corrections to the tree level Higgs potential, which include the contributions from various particles and sparticles with sizeable Yukawa and/or gauge couplings to the Higgs sector. Explicit forms for the \( \Sigma_u \) and \( \Sigma_d \) are given in the Appendix of Ref. Obviously, in order to get the observed value of \( M_Z \) without finely tuned cancellations in Eq. (1), each term on the right-hand side should be comparable in magnitude. This then suggests that the electroweak fine-tuning of \( M_Z^2 \) can be quantified by \( \Delta_{EW}^{-1} \),

\[ \Delta_{EW}^{-1} \equiv (M_Z^2/2)/\max_i |C_i|. \]

(2)

Here, \( C_{H_u} = -m^2_{H_u} \tan^2 \beta/(\tan^2 \beta - 1) \), \( C_{H_d} = m^2_{H_d}/(\tan^2 \beta - 1) \) and \( C_\mu = -\mu^2 \). Also, \( C_{\Sigma_u(i)} = -\Sigma_u(i)/(\tan^2 \beta - 1) \) and \( C_{\Sigma_d(i)} = \Sigma_d(i)/(\tan^2 \beta - 1) \), where \( i \) labels the various loop contributions to \( \Sigma_u \) and \( \Sigma_d \). So an upper bound on \( \Delta_{EW}^{-1} \gtrsim 10\% \) from naturalness considerations implies that the higgsino mass parameter \( \mu \) must be of the order of \( \sim 100-200 \) GeV. Hence, to probe the SUSY naturalness at LHC, the most essential task is to search for light higgsinos. However, due to the low (percent level) signal-to-background ratio, detecting the pair production of these nearly degenerate higgsinos through monojet(-like) or vector boson fusion events seems challenging at LHC [4–6].

Besides higgsinos, the stops usually strongly relate with the naturalness, which can contribute to \( \Delta_{EW}^{-1} \) at one-loop level and favor the stop mass not to be too heavy\(^2\) [7]. In

\(^1\) The Barbieri and Guidice (BG) measure in Ref. [2] is applicable to a theory with several independent effective theory parameters. But for a more fundamental theory, BG measure often leads to over-estimates of fine tuning [3].

\(^2\) In some supersymmetric models, such as Ref. [8], the bound on the stop mass from naturalness can be weakened due to the cancellation between stop loop and other sparticle loops.
addition, there are other good theoretical motivations of considering a light stop. For example, in some popular grand unification models, supersymmetry breaking is usually assumed to transmit to the visible sector at a certain high energy scale, and then Yukawa contributions to the renormalization group evolution tend to reduce stop masses more than other squark masses. Another one is that the chiral mixing for certain flavor squarks is proportional to the mass of the corresponding quark, and is therefore more sizable for stops. Such a mixing will further reduce the mass of the lighter stop. Moreover, we note that a light stop is phenomenologically needed by the electroweak baryogenesis [9]. Given these, the searches for pair/single production of stop are also important to understand the naturalness and to test supersymmetric models at LHC [10–12].

So far, experimental searches for stops at LHC Run-1 have resulted in bounds on stop masses of a few hundred GeV [13–23]. The present search strategies of the direct stop pair production mainly depend on the mass splitting between the stop and the lightest supersymmetric partner (LSP). For example, when \(\Delta m_{\tilde{t}_1 - \tilde{\chi}_1^0} \gg m_t\), the top quark from stop decay can be quite energetic as compared with the top quarks in the \(t\bar{t}\) background. Therefore, certain endpoint observables, like \(M_{T_2}\), can be used to efficiently reduce the \(t\bar{t}\) background [14, 16, 17, 22, 23]. Contrary to this, in the compressed region, where \(\Delta m_{\tilde{t}_1 - \tilde{\chi}_1^0} \approx m_t\), the kinematics of the top quarks from stop decay are similar to those in the top pair production and the standard search strategies often suffer from a poor sensitivity. For this case, one way is to compare the top pair production cross section measurement with the theoretical prediction, which can rule out stop masses below \(\sim 180\) GeV for a light neutralino LSP [15, 24, 25]. Another way is to use a high momentum jet recoiling against \(\tilde{t}_1\tilde{t}_1^*\) system to produce the large \(E_T^{miss}\) and anti-correlation between \(E_T^{miss}\) and the recoil jet transverse vectors [26–28]. Furthermore, if \(\Delta m_{\tilde{t}_1 - \tilde{\chi}_1^0} \ll m_t\), the stop decay will be dominated by the four-body channel \(\tilde{t}_1 \rightarrow b f' \tilde{\chi}_1^0\) or the two-body loop channel \(\tilde{t}_1 \rightarrow c \chi_1^0\) [29–32]. But due to the small mass difference, the decay products of the stop are usually too soft to be observed. Thus the single high \(p_T\) hard jet from the ISR/FSR (with the heavy quark tagging) is used to tag these compressed stop events [33–36]. At the same time, many theoretical studies have been devoted to improving the LHC sensitivity to the stop searches in some special kinematical regions [37] and to constraining the light stops in various theoretical frameworks [38].

Besides the sparticle mass splitting, the assumption on the branching ratios of stop and
the nature of neutralinos can significantly affect the sensitivity of the LHC direct searches. For example, if $M_{1,2} \gg \mu$, the left-handed stop decay $\tilde{t}_1 \to t\tilde{\chi}^0_{1,2}$ is enhanced by the large top quark Yukawa coupling. Also, due to the $SU(2)$ symmetry and nearly degenerate higgsinos ($\tilde{\chi}^0_{1,2}$ and $\tilde{\chi}^1_1$), the left-handed sbottom decays $\tilde{b}_1 \to t\tilde{\chi}^-_{1,1}$ inevitably mimics the stop signals $\tilde{t}_1 \to t\tilde{\chi}^0_{1,2}$. The combined null results of the stop and sbottom searches have excluded a left-handed stop below about 600 GeV in natural SUSY scenario [39–42]. On the other hand, since the right-handed stop has no $SU(2)$ gauge symmetry link with the sbottom sector, sbottoms can be decoupled and will not necessarily contribute to the stop events. Thus, the LHC direct search constraints on the right-handed stop will become weaker, and may still allow stop mass around the weak scale.

In this work, we use the LHC Run-1 data to determine the lower mass limit of the right-handed stop in a natural SUSY scenario, where the higgsinos $\tilde{\chi}^0_{1,2}$ and $\tilde{\chi}^\pm_1$ are light and nearly degenerate in mass ($2 \text{ GeV} \lesssim \Delta m \lesssim 5 \text{ GeV}$). Then we investigate the prospect of closing up the currently allowed light right-handed stop mass region through the direct searches for $2b + E_T^{\text{miss}}$, $1\ell + jets + E_T^{\text{miss}}$ and monojet events at 14 TeV LHC. Apart from the direct searches, one may also utilise indirect observations to constrain the light stops. Namely, the light stops can significantly affect the loop processes $gg \to h$ and $h \to \gamma\gamma$. With the upgrade of LHC, the Higgs couplings with the gauge bosons will be measured with much higher experimental accuracy than the current measurements and may be used to indirectly constrain our scenario. We also explore the potential of the Higgs golden ratio $D_{\gamma\gamma} = \sigma(pp \to h \to \gamma\gamma)/\sigma(pp \to h \to ZZ^* \to 4\ell^\pm)$ [44] as a complementary probe for the light stop scenario.

II. CALCULATIONS, RESULTS AND DISCUSSION

Considering the higgsinos and stops are closely related to the naturalness problem, we scan the following region of the MSSM parameter space:

$$
100 \text{ GeV} \leq \mu \leq 300 \text{ GeV}, \quad 100 \text{ GeV} \leq m_{\tilde{t}_R} \leq 1 \text{ TeV}, \\
1.5 \text{ TeV} \leq m_{\tilde{Q}_{3L}} \leq 3 \text{ TeV}, \quad 1 \text{ TeV} \leq A_t \leq 3 \text{ TeV}, \quad 5 \leq \tan\beta \leq 50.
$$ (3)
As our study is performed in a simplified phenomenological MSSM, we abandon the relation
\( M_1 : M_2 : M_3 = 1 : 2 : 7 \) inspired the gaugino mass unification \(^3\) and assume \( M_1 = M_2 = 2 \)
TeV at the weak scale for simplicity. Such a condition leads to the nearly degenerate
higgsinos (with the mass splitting around 2-5 GeV). Besides, in order to avoid introducing
too much fine-tuning, we take \( M_3 = 1.5 \) TeV, which usually contributes to the Higgs mass
at two-loop level. The sleptons and the first two generations of squarks in natural SUSY
are supposed to be heavy to avoid the SUSY flavor and CP problems, which are all fixed
at 3 TeV. We also assume \( m_A = 1 \) TeV, \( A_b = 0 \) and \( m_{\tilde{b}_R} = 2 \) TeV. Such a setup will make
our lighter stop \( \tilde{t}_1 \) dominated by the right-handed component, and also provide the correct
Higgs mass. In our scan we consider the following constraints:

A. Indirect Constraints

(1) We choose the light CP-even Higgs boson as the SM-like Higgs boson and require
its mass in the range of 123–127 GeV. We use the package of \textit{FeynHiggs-2.11.2} \(^4\) to calculate the Higgs mass \(^4\). Besides, a light stop with the large mixing trilinear
parameter \( A_t \) needed by the Higgs mass often leads to a global vacuum where charge
and colour are broken \([49, 50]\). We impose the constraint of the metastability of the
vacuum state by requiring \( |A_t| \lesssim 2.67\sqrt{M_{Q^3_{3L}}^2 + M_{\tilde{t}_R}^2 + M_A^2 \cos^2 \beta} \) \([50]\).

(2) Since the light stop and higgsinos can contribute to the B-physics observables, we
require our samples to satisfy the bound of \( B \rightarrow X_s \gamma \) at 2\(\sigma\) level. We use the package
of \textit{SuperIso v3.3} \([51]\) to implement this constraint.

(3) As known, in the natural MSSM, the thermal relic density of the light higgsino-like
neutralino dark matter is typically low because of the large annihilation rate in the
early universe. In order to provide the required relic density, several alternative ways

\(^3\) Note that one possible way to relax the naturalness problem is to choose a suitable boundary condition
of gaugino masses at the GUT scale, such as \( M_2 : M_3 \simeq 5 : 1 \) in Ref. \([45]\).

\(^4\) In general, different packages may give a different Higgs mass prediction. It is known from the MSSM
that spectrum generators performing a \( \overline{DR} \) calculation (such as Suspect \([47]\)) can agree quite well, while
sizable differences to the OS calculation of \textit{FeynHiggs} exists. The differences are assumed to arise from
the missing electroweak corrections and momentum dependence at two-loop level as well as from the
dominant three-loop corrections. These are the effects that underlie the often-quoted estimate of a few
GeV uncertainty for the SM-like Higgs mass in the MSSM \([48]\).
have been proposed [52–54], such as choosing the axion-higgsino admixture as the dark matter [55]. However, if the naturalness requirement is relaxed, the heavy higgsino-like neutralino with a mass about 1 TeV can solely produce the correct relic density in the MSSM [56]. So we require the thermal relic density of the neutralino dark matter is below the $2\sigma$ upper limit of the Planck value [57]. We use the package of $\text{MicrOmega}$ v2.4 [58] to calculate the relic density.

We have also verified using $\text{HiggsBounds}$-4.2.1 [59] and $\text{HiggsSignals}$-1.4.0 [60] packages that the samples allowed by the above constraints are also consistent with the Higgs data from LEP, Tevatron and LHC.

![FIG. 1: Dependence of the stop decay branching ratio on the mass splitting $\Delta m_{\tilde{t}_1 - \tilde{\chi}_1^0}$.](image)

In Fig.1, we show the dependence of the stop decay branching ratios on the mass splitting $\Delta m_{\tilde{t}_1 - \tilde{\chi}_1^0}$ in our scenario. The branching ratios are calculated by the package of $\text{SDECAY}$ [61]. We can see that a heavy right-handed stop decays to $b\tilde{\chi}_1^+$ with $Br \simeq 50\%$ and $t\tilde{\chi}_1^0$ with $Br \simeq 25\%, 25\%$. This is because the partial decay width $\Gamma(\tilde{t}_1 \rightarrow b\tilde{\chi}_1^+)$ and $\Gamma(\tilde{t}_1 \rightarrow t\tilde{\chi}_1^0)$ are both proportional to $y_t^2$ ($y_t$ is the top quark Yukawa coupling) [30]. Other decay modes $\tilde{t}_1 \rightarrow t\tilde{\chi}_{3,4}^0$ are kinematically forbidden because the bino and wino mass is assumed to be decoupled in our calculations. For $m_b + m_W < \Delta m_{\tilde{t}_1 - \tilde{\chi}_1^0} < m_t$, the dominant decay process is still $\tilde{t}_1 \rightarrow b\tilde{\chi}_1^+$ because it has a much larger phase space than the three-body decay channel $\tilde{t}_1 \rightarrow bW\tilde{\chi}_1^0$. Further, if $\Delta m_{\tilde{t}_1 - \tilde{\chi}_1^0} < m_b + m_W$, the four-body decay process $\tilde{t}_1 \rightarrow bf\bar{f}\tilde{\chi}_1^0$ and the loop decay channel $\tilde{t}_1 \rightarrow c\tilde{\chi}_1^0$ are extremely suppressed (except for the region where $\tilde{t}_1 \rightarrow b\tilde{\chi}_1^+$ is kinematically forbidden), as shown in Fig.1. The reason is that our stop is
TABLE I: The signals of the LHC stop direct searches and the corresponding sources in the natural SUSY.

| LHC stop direct searches | Sources in natural SUSY |
|-------------------------|-------------------------|
| $\ell + jets + E_T^{miss}$ [14, 22] | $pp \rightarrow \tilde{t}_1\tilde{t}_1 (\tilde{t}_1 \rightarrow t\tilde{\chi}^0_{1,2})$ |
| $2b + E_T^{miss}$ [18] | $pp \rightarrow \tilde{t}_1\tilde{t}_1 (\tilde{t}_1 \rightarrow b\tilde{\chi}^+_1)$ |
| $jet + E_T^{miss}$ [13] | $pp \rightarrow jet + \tilde{t}_1\tilde{t}_1 (\tilde{t}_1 \rightarrow b\tilde{\chi}^+_1, b\tilde{f}\tilde{f}^{*}\tilde{\chi}^0_{1,2}, c\tilde{\chi}^0_{1,2})$ |

predominantly right-handed and the neutralino $\tilde{\chi}^0_1$ is higgsino-like, so that the decay width of $\tilde{t}_1 \rightarrow c\tilde{\chi}^0_1$ is heavily reduced because of tiny $\tilde{t}_L,R - \tilde{c}_L$ mixing and of the gaugino-higgsino nature of neutralinos [29]. The decay $\tilde{t}_1 \rightarrow b\tilde{f}\tilde{f}^{*}\tilde{\chi}^0_1$ is also suppressed due to the small phase space (note that the neutralinos $\tilde{\chi}^0_{1,2}$ and the chargino $\tilde{\chi}^+_1$ are nearly degenerate higgsinos).

B. Direct Constraints

In our scenario, due to $M_{1,2} \gg \mu$, the higgsinos $\tilde{\chi}^\pm_1$ and $\tilde{\chi}^0_{1,2}$ are nearly degenerate so that their decay products are too soft to be tagged at LHC. Such a feature can change the conventional LHC signatures in some certain stop decay channels. For example, the stop pair production followed by the dominant decay $\tilde{t}_1 \rightarrow b\tilde{f}\tilde{f}^{*}\tilde{\chi}^0_1$ will appear as $2b + E_T^{miss}$. So in our study, we consider the following relevant LHC direct search constraints at $\sqrt{s} = 8$ TeV:

1. The ATLAS search for stop/sbottom pair production in final states with missing transverse momentum and two b-jets [18].

2. The ATLAS and CMS search for stop pair production in final states with one isolated lepton, jets, and missing transverse momentum [14, 22];

3. The ATLAS search for pair-produced stops decaying to charm quark or in compressed supersymmetric scenarios [13].

In Table II B, we summarize the signals of the above direct searches and the corresponding source of each signal in our scenario. We use the packages CheckMATE-1.2.1 [62] and MadAnalysis 5-1.1.12 [63] to recast the above ATLAS analyses (1)-(3) and CMS analysis (2), respectively. We calculate the NLO+NLL cross section of the stop pair production by using NLL-fast package [64] with the CTEQ6.6M PDFs [65]. The parton level signal events are
generated by the package MadGraph5 [66] and are showered and hadronized by the package PYTHIA [67]. The detector simulation effects are implemented with the tuned package Delphes [68], which is included in CheckMATE-1.2.1 and MadAnalysis 5-1.1.12. The jets are clustered with the anti-kt algorithm [69] by the package FastJet [70]. Finally, we define the ratio $r = \max(N_{S,i}/S_{95\%}^{obs,i})$ for each experimental search. Here $N_{S,i}$ is the number of the signal events for the $i$-th signal region and $S_{95\%}^{obs,i}$ is the corresponding observed 95% C.L. upper limit. The $\max$ is over all the signal regions for each search. If $r > 1$, we conclude that such a point is excluded at 95% C.L..

C. Results

![Regions excluded by the direct searches for the stop pair at 8 TeV run (left panel) and extrapolation to the 14 TeV run (right panel) with $\mathcal{L} = 20 \text{ fb}^{-1}$](image)

**FIG. 2**: Regions excluded by the direct searches for the stop pair at 8 TeV run (left panel) and extrapolation to the 14 TeV run (right panel) with $\mathcal{L} = 20 \text{ fb}^{-1}$. For $1\ell + \text{jets} + E_T^{\text{miss}}$ and $2b + E_T^{\text{miss}}$, the region below each curve is the excluded region. For the monojet search, the region to the left of the curve is its excluded region. The green crosses represent the samples allowed by the current indirect and direct constraints.

In Fig.2, we plot the exclusion limits of the direct searches for the stop pair in the plane of $m_{\tilde{t}_1}$ versus LSP mass at 8 TeV LHC with $\mathcal{L} = 20 \text{ fb}^{-1}$. The green crosses represent the samples allowed by the current indirect and direct constraints. Since the moderate or heavy right-handed stop dominantly decays to $b\tilde{\chi}_1^+$ and $t\tilde{\chi}_{1,2}^0$, which produces $2b + E_T^{\text{miss}}$.
and $t\bar{t} + E_T^{\text{miss}}$ signatures respectively, we can see that the searches for $2b + E_T^{\text{miss}}$ and $1\ell + jets + E_T^{\text{miss}}$ events give strong bounds on the stop mass in the region with $\Delta m_{\tilde{t}_1 - \tilde{\chi}_1^0} > m_t$.

For example, when $\mu \simeq 100$ (250) GeV, the stop mass has been excluded up to about 540 (430) GeV by $1\ell + jets + E_T^{\text{miss}}$ ($2b + E_T^{\text{miss}}$). If the stop mass is close to the LSP mass, the $b$-jets from the stop decay $\tilde{t}_1 \to b\tilde{\chi}_1^+ / b\tilde{f}\tilde{\chi}^0_{1,2}$ or $c$-jets from $\tilde{t}_1 \to c\tilde{\chi}_1^0$ become soft. Then the monojet search will be a sensitive probe for this region and can exclude the stop mass up to 150 GeV for $\mu \simeq 100$ GeV. While in a small strip of parameter space with $m_{\tilde{\chi}_1^0} \gtrsim 190$ GeV, the stop mass can still be as light as 210 GeV and compatible with all the current bounds. As pointed in [71], the higher energy will improve the sensitivity of the monojet searches for a mass splitting below 100 GeV. So, we regenerate the corresponding signals and backgrounds, and extrapolate our analyses to 14 TeV LHC by taking the same cut values and the definitions of the signal regions as those at 8 TeV LHC $^5$. Then, we can see that such a narrow region for a light stop can be further covered by the constraints of monojet and $2b + E_T^{\text{miss}}$ with 20 fb$^{-1}$ of data. At the same time, the lower bound of the stop mass will be pushed up to about 660 GeV for $m_{\tilde{\chi}_1^0} \lesssim 330$ GeV and 710 GeV for $m_{\tilde{\chi}_1^0} \sim 100$ GeV by $2b + E_T^{\text{miss}}$ and $1\ell + jets + E_T^{\text{miss}}$ searches, respectively.

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{constraint.png}
\caption{Constraints of the Higgs golden ratio $D_{\gamma\gamma} = \sigma(pp \to h \to \gamma\gamma) / \sigma(pp \to h \to ZZ^* \to 4\ell^\pm)$ on the light stop shown in the left panel of Fig.2. The colormap represents the mass difference between the stop and the LSP.
}
\end{figure}

$^5$ Here we conservatively estimate the exclusion limits at 14 TeV LHC. The optimization of the cut values and the signal regions may further improve our results.
On the other hand, with more data collected at the LHC, the precision measurement of Higgs couplings can be used as indirect probes of light new particles. In natural SUSY, the stops may significantly change the loop processes $gg \rightarrow h$ and $h \rightarrow \gamma\gamma$. However, the signal strength measurement of $pp \rightarrow h \rightarrow \gamma\gamma$ suffers from some theoretical uncertainties [73]. To solve this problem, a high-precision Higgs observable $D_{\gamma\gamma}$ that can be measured at percent level was constructed by using the ratio of the Higgs golden channel signal strengths [44],

$$D_{\gamma\gamma} = \frac{\mu(pp \rightarrow h \rightarrow \gamma\gamma)}{\mu(pp \rightarrow h \rightarrow ZZ^* \rightarrow 4\ell^{\pm})}.$$

In Fig.3, we present the constraints of the Higgs golden ratio $D_{\gamma\gamma}$ on the light stop window shown in Fig.2. It can be seen that the stop with mass $m_{\tilde{t}_1} \simeq m_t$ can significantly reduce the value of $D_{\gamma\gamma}$ by about 18% because such a light stop will cancel with the contribution of $W$-loop in the decay of $h \rightarrow \gamma\gamma$. While with the increase of the stop mass, the contribution of the stop loop can change the sign and constructively interfere with the $W$-loop. On the other hand, since the decay width of $h \rightarrow \gamma\gamma$ also depends on the trilinear parameter $A_t$ and $\tan \beta$ [74], some of our samples can make $D_{\gamma\gamma}$ very close to 1. Therefore, if the golden ratio $D_{\gamma\gamma}$ can be measured at 1% level (as discussed in [44]) at the HL-LHC or future $e^+e^-$ colliders, most of our light stop region allowed by 8 TeV LHC can be excluded.

III. CONCLUSIONS

In this work we used the LHC Run-1 data to constrain the right-handed stop in a natural SUSY scenario, where the higgsinos $\tilde{\chi}^0_{1,2}$ and $\tilde{\chi}^\pm_1$ are light ($\mu \simeq 100 - 300$ GeV) and nearly degenerate. For $m_{\tilde{t}_1} \gg m_t$, we found that the stop mass is excluded up to about 540 (430) GeV for $\mu \simeq 100$ (250) GeV by the 8 TeV LHC direct searches in $1\ell + jets + E_T^{miss}$ ($2b + E_T^{miss}$) channel. However, in a small strip of parameter space with $m_{\tilde{\chi}^0_1} \gtrsim 190$ GeV, the stop mass can still be as light as 210 GeV and compatible with the bounds from the Higgs mass and the current monojet searches. We have extrapolated our analyses to 14 TeV LHC and found that such a light stop mass window can be further covered by the monojet and $2b + E_T^{miss}$ searches. The lower bound of the stop mass will be pushed up to about 710 GeV. We also found that the precision measurement of the Higgs golden ratio $D_{\gamma\gamma} = \sigma(pp \rightarrow h \rightarrow \gamma\gamma)/\sigma(pp \rightarrow h \rightarrow ZZ^* \rightarrow 4\ell^{\pm})$ at percent level can exclude most of our light stop region and thus play a complementary role in probing the light stop.
Acknowledgments

We thank Manuel Drees and Jong Song Kim for helpful discussions. This work is partly supported by the Australian Research Council, by the National Natural Science Foundation of China (NNSFC) under grants Nos. 11275057, 11305049, 11375001, 11405047, 11135003, 11275245, by Specialised Research Fund for the Doctoral Program of Higher Education under Grant No. 20134104120002, by the Startup Foundation for Doctors of Henan Normal University under contract No.11112, and the Joint Funds of the National Natural Science Foundation of China (U1404113).

[1] R. Arnowitt and P. Nath, Phys. Rev. D 46, 3981 (1992).
[2] R. Barbieri and G. F. Giudice, Nucl. Phys. B 306, 63 (1988).
[3] H. Baer, V. Barger and D. Mickelson, Phys. Rev. D 88, no. 9, 095013 (2013); H. Baer, V. Barger, D. Mickelson and M. Padeffke-Kirkland, Phys. Rev. D 89, no. 11, 115019 (2014).
[4] G. F. Giudice and A. Pomarol, Phys. Lett. B 372, 253 (1996); G. F. Giudice, T. Han, K. Wang and L. T. Wang, Phys. Rev. D 81, 115011 (2010); H. Baer, V. Barger and P. Huang, JHEP 1111, 031 (2011); S. Gori, S. Jung and L. T. Wang, JHEP 1310, 191 (2013);
[5] C. Han, et al., JHEP 1402, 049 (2014); P. Schwaller and J. Zurita, JHEP 1403, 060 (2014); Z. Han, G. D. Kribs, A. Martin and A. Menon, Phys. Rev. D 89, 075007 (2014); H. Baer, A. Mustafayev and X. Tata, Phys. Rev. D 89, no. 5, 055007 (2014); Phys. Rev. D 90, 115007 (2014); C. Han, D. Kim, S. Munir and M. Park, JHEP 1504, 132 (2015); D. Barducci, et al., arXiv:1504.02472 [hep-ph];
[6] A. G. Delannoy, et al., Phys. Rev. Lett. 111, 061801 (2013); A. Arbey, M. Battaglia and F. Mahmoudi, Phys. Rev. D 89, 077701 (2014); J. Bramante, et al., Phys. Rev. D 90, 095008 (2014); A. Anandakrishnan, L. M. Carpenter and S. Raby, Phys. Rev. D 90, 055004 (2014); C. Han, et al., Phys. Rev. D 91, 055030 (2015); P. Stengel and X. Tata, arXiv:1507.06726 [hep-ph]; W. Abdallah, J. Fiaschi, S. Khalil and S. Moretti, Phys. Rev. D 92, 055029 (2015); arXiv:1510.06475 [hep-ph]; M. Badziak, et al., arXiv:1506.07177 [hep-ph]; T. Liu, L. Wang and J. M. Yang, JHEP 1502, 177 (2015); A. Kobakhidze and M. Talia, arXiv:1508.04068 [hep-ph].
[7] S. F. King, M. Muhlleitner and R. Nevzorov, Nucl. Phys. B 860, 207 (2012).
[8] S. P. Martin, Phys. Rev. D 79, 095019 (2009); J. E. Younkin and S. P. Martin, Phys. Rev. D 85 (2012) 055028; S. Akula and P. Nath, Phys. Rev. D 87, 115022 (2013); I. Gogoladze, F. Nasir and Q. Shafi, Int. J. Mod. Phys. A 28, 1350046 (2013).
[9] P. Huet and A. E. Nelson, Phys. Rev. D 53 (1996) 4578; M. Carena, G. Nardini, M. Quiros and C. E. M. Wagner, Nucl. Phys. B 812 (2009) 243; Y. Li, S. Profumo and M. Ramsey-Musolf, Phys. Lett. B 673 (2009) 95.
[10] C. Brust, A. Katz, S. Lawrence and R. Sundrum, JHEP 1203, 103 (2012).
[11] H. Baer, V. Barger and M. Savoy, arXiv:1509.02929 [hep-ph].
[12] J. Cao, et al., JHEP 1211, 039 (2012). A. Kobakhidze, N. Liu, L. Wu and J. M. Yang, Phys. Rev. D 92, 075008 (2015); K. Hikasa, J. Li, L. Wu and J. M. Yang, arXiv:1505.06006 [hep-ph].
[13] G. Aad et al. [ATLAS Collaboration], Phys. Rev. D 90, 052008 (2014).
[14] G. Aad et al. [ATLAS Collaboration], JHEP 1411, 118 (2014).
[15] G. Aad et al. [ATLAS Collaboration], Eur. Phys. J. C 74, 3109 (2014).
[16] G. Aad et al. [ATLAS Collaboration], JHEP 1409, 015 (2014).
[17] G. Aad et al. [ATLAS Collaboration], JHEP 1406, 124 (2014).
[18] G. Aad et al. [ATLAS Collaboration], JHEP 1310, 189 (2013).
[19] S. Chatrchyan et al. [CMS Collaboration], Phys. Rev. Lett. 112, 161802 (2014).
[20] S. Chatrchyan et al. [CMS Collaboration], Phys. Lett. B 736, 371 (2014).
[21] S. Chatrchyan et al. [CMS Collaboration], Phys. Lett. B 743, 503 (2015).
[22] S. Chatrchyan et al. [CMS Collaboration], Eur. Phys. J. C 73, 2677 (2013).
[23] S. Chatrchyan et al. [CMS Collaboration], arXiv:1503.08037 [hep-ex].
[24] X. Q. Li, et al. Phys. Rev. D 89, 077703 (2014).
[25] M. Czakon, et al., Phys. Rev. Lett. 113, 201803 (2014).
[26] H. An and L. T. Wang, Phys. Rev. Lett. 115, 181602 (2015).
[27] S. Macaluso, M. Park, D. Shih and B. Tweedie, arXiv:1506.07885 [hep-ph].
[28] K. Hagiwara and T. Yamada, Phys. Rev. D 91, 094007 (2015).
[29] K. Hikasa and M. Kobayashi, Phys. Rev. D 36, 724 (1987); T. Han, K. Hikasa, J. M. Yang and X. Zhang, Phys. Rev. D 70, 055001 (2004).
[30] A. Djouadi and Y. Mambrini, Phys. Rev. D 63, 115005 (2001); C. Boehm, A. Djouadi and Y. Mambrini, Phys. Rev. D 61, 095006 (2000).
[31] R. Grober, M. M. Muhlleitner, E. Popenda and A. Wlotzka, Eur. Phys. J. C 75, no. 9, 420 (2015); M. Muhlleitner and E. Popenda, JHEP 1104, 095 (2011); R. Grober, M. Muhlleitner, E. Popenda and A. Wlotzka, Phys. Lett. B 747, 144 (2015).

[32] J. Aebischer, A. Crivellin and C. Greub, Phys. Rev. D 91, no. 3, 035010 (2015) [arXiv:1410.8459 [hep-ph]].

[33] M. Drees, M. Hanussek and J. S. Kim, Phys. Rev. D 86, 035024 (2012).

[34] A. Choudhury and A. Datta, Mod. Phys. Lett. A 27, 1250188 (2012).

[35] Z. H. Yu, X. J. Bi, Q. S. Yan and P. F. Yin, Phys. Rev. D 87, no. 5, 055007 (2013).

[36] M. A. Ajaib, T. Li and Q. Shafi, Phys. Rev. D 85, 055021 (2012).

[37] T. Plehn, M. Spannowsky, M. Takeuchi and D. Zerwas, JHEP 1010, 078 (2010); D. E. Kaplan, K. Rehermann and D. Stolarski, JHEP 1207, 119 (2012); T. Plehn, M. Spannowsky and M. Takeuchi, JHEP 1208, 091 (2012); Phys. Rev. D 85, 034029 (2012); JHEP 1105, 135 (2011); J. Thaler and K. Van Tilburg, JHEP 1202, 093 (2012); Z. Han, A. Katz, D. Krohn and M. Reece, JHEP 1208, 083 (2012); Y. Bai, H. C. Cheng, J. Gallicchio and J. Gu, JHEP 1207, 110 (2012); JHEP 1308, 085 (2013); D. S. M. Alves et al., Phys. Rev. D 87, 035016 (2013); M. L. Graesser and J. Shelton, Phys. Rev. Lett. 111, 121802 (2013); B. Nachman and C. G. Lester, Phys. Rev. D 88, 075013 (2013); G. Belanger, et al., Phys. Rev. D 89, 015003 (2014); B. Fuks, P. Richardson and A. Wilcock, Eur. Phys. J. C 75, 308 (2015); G. Belanger, D. Ghosh, R. Godbole and S. Kulkarni, JHEP 1509, 214 (2015); R. Huo, arXiv:1509.05942 [hep-ph]; T. Eifert and B. Nachman, Phys. Lett. B 743, 218 (2015); A. Ismail, R. Schwienhorst, J. S. Virzi and D. G. E. Walker, Phys. Rev. D 91, 074002 (2015); B. Batell and S. Jung, JHEP 1507, 061 (2015); M. Backovic, A. Mariotti and M. Spannowsky, JHEP 1506, 122 (2015); W. S. Cho, et al., JHEP 1505, 040 (2015); J. H. Collins, J. A. Dror and M. Farina, arXiv:1508.02419 [hep-ph]. G. Ferretti, R. Franceschini, C. Petersson and R. Torre, arXiv:1502.01721 [hep-ph].

[38] X. J. Bi, Q. S. Yan and P. F. Yin, Phys. Rev. D 85, 035005 (2012); Phys. Rev. D 87, 035007 (2013); T. Cheng, J. Li, T. Li and Q. S. Yan, Phys. Rev. D 89, 015015 (2014); B. Kaufman, P. Nath, B. D. Nelson and A. B. Spisak, arXiv:1509.02530 [hep-ph]; A. Belyaev, V. Sanz and M. Thomas, arXiv:1510.07688 [hep-ph]; H. Abe, J. Kawamura and Y. Omura, JHEP 1508, 089 (2015); A. Chakraborty, et al., Phys. Rev. D 91, 115018 (2015); S. Chakraborty, et al., arXiv:1508.01875 [hep-ph]; J. Beuria, A. Chatterjee, A. Datta and S. K. Rai, JHEP 1509, 13.
073 (2015);
[39] L. J. Hall, D. Pinner and J. T. Ruderman, JHEP 1204, 131 (2012); M. Papucci, J. T. Ruderman and A. Weiler, JHEP 1209, 035 (2012).
[40] G. D. Kribs, A. Martin and A. Menon, Phys. Rev. D 88, 035025 (2013).
[41] C. Han, et al., JHEP 1310, 216 (2013).
[42] K. Kowalska and E. M. Sessolo, Phys. Rev. D 88, no. 7, 075001 (2013) [arXiv:1307.5790 [hep-ph]].
[43] [ATLAS Collaboration], arXiv:1307.7292 [hep-ex]; [CMS Collaboration], arXiv:1307.7135.
[44] A. Djouadi, J. Quevillon and R. Vega-Morales, arXiv:1509.03913 [hep-ph].
[45] H. Abe, T. Kobayashi and Y. Omura, Phys. Rev. D 76, 015002 (2007) doi:10.1103/PhysRevD.76.015002 [hep-ph/0703044 [HEP-PH]].
[46] S. Heinemeyer, W. Hollik and G. Weiglein, Comput. Phys. Commun. 124, 76 (2000); Eur. Phys. J. C 9, 343 (1999).
[47] A. Djouadi, J. -L. Kneur and G. Moultaka, Comput. Phys. Commun. 176, 426 (2007).
[48] J. P. Vega and G. Villadoro, JHEP 1507, 159 (2015) doi:10.1007/JHEP07(2015)159;
[49] J. E. Camargo-Molina, B. O’Leary, W. Porod and F. Staub, JHEP 1312, 103 (2013); N. Blinov and D. E. Morrissey, JHEP 1403, 106 (2014); J. E. Camargo-Molina, B. Garbrecht, B. O’Leary, W. Porod and F. Staub, Phys. Lett. B 737, 156 (2014); N. Chamoun, H. K. Dreiner, F. Staub and T. Stefaniak, JHEP 1408, 142 (2014); U. Chattopadhyay and A. Dey, JHEP 1411, 161 (2014);
[50] D. Chowdhury, R. M. Godbole, K. A. Mohan and S. K. Vempati, JHEP 1402, 110 (2014).
[51] F. Mahmoudi, Comput. Phys. Commun. 180, 1579 (2009); Comput. Phys. Commun. 178, 745 (2008).
[52] B. S. Acharya, G. Kane and E. Kuflik, arXiv:1006.3272 [hep-ph].
[53] T. Moroi and L. Randall, Nucl. Phys. B 570, 455 (2000); G. Gelmini and P. Gondolo, Phys. Rev. D 74, 023510 (2006); B. Acharya, et al., Phys. Rev. D 76, 126010 (2007); Phys. Rev. D 78, 065038 (2008).
[54] K-Y. Choi, J. E. Kim, H. M. Lee and O. Seto, Phys. Rev. D 77, 123501 (2008).
[55] H. Baer, A. Lessa, S. Rajagopalan and W. Sreethawong, JCAP 1106 (2011) 031; H. Baer, A. Lessa and W. Sreethawong, JCAP 1201 (2012) 036.
[56] U. Chattopadhyay and D. P. Roy, Phys. Rev. D 68, 033010 (2003); U. Chattopadhyay, et al.,
Phys. Lett. B 632, 114 (2006).

[57] P. A. R. Ade et al. [Planck Collaboration], arXiv:1303.5076 [astro-ph.CO].

[58] G. Belanger et al., Comput. Phys. Commun. 182, 842 (2011).

[59] P. Bechtle et al., Comput. Phys. Commun. 182, 2605 (2011); Comput. Phys. Commun. 181, 138 (2010).

[60] P. Bechtle et al., Eur. Phys. J. C 74, 2711 (2014); P. Bechtle et al., Comput. Phys. Commun. 181, 138 (2010).

[61] M. Muhlleitner, A. Djouadi and Y. Mambrini, Comput. Phys. Commun. 168, 46 (2005).

[62] M. Drees et al., Comput. Phys. Commun. 187, 222 (2013); J. S. Kim et al., arXiv:1503.01123 [hep-ph].

[63] E. Conte, B. Fuks and G. Serret, Comput. Phys. Commun. 184, 222 (2013); E. Conte, B. Dumont, B. Fuks and C. Wymant, Eur. Phys. J. C 74, no. 10, 3103 (2014); B. Dumont et al., Eur. Phys. J. C 75, 56 (2015).

[64] W. Beenakker et al., Int. J. Mod. Phys. A 26, 2637 (2011); A. Kulesza and L. Motyka, Phys. Rev. D 80, 095004 (2009); W. Beenakker et al., JHEP 0912, 041 (2009); A. Kulesza and L. Motyka, Phys. Rev. Lett. 102, 111802 (2009); W. Beenakker, R. Hopker, M. Spira and P. M. Zerwas, Nucl. Phys. B 492, 51 (1997).

[65] D. Stump et al., JHEP 0310, 046 (2003) [hep-ph/0303013].

[66] J. Alwall et al., JHEP 1106, 128 (2011).

[67] T. Sjostrand, S. Mrenna and P. Z. Skands, JHEP 0605, 026 (2006).

[68] J. de Favereau et al. [DELPHES 3 Collaboration], JHEP 1402, 057 (2014).

[69] M. Cacciari, G. P. Salam and G. Soyez, JHEP 0804, 063 (2008).

[70] M. Cacciari, G. P. Salam and G. Soyez, Eur. Phys. J. C 72, 1896 (2012).

[71] A. Arbey, M. Battaglia and F. Mahmoudi, arXiv:1506.02148 [hep-ph].

[72] K. J. Bae, H. Baer, N. Nagata and H. Serce, Phys. Rev. D 92, 035006 (2015).

[73] S. Dittmaier et al. [LHC Higgs Cross Section Working Group Collaboration], arXiv:1101.0593 [hep-ph].

[74] J. Cao, L. Wu, P. Wu and J. M. Yang, JHEP 1309, 043 (2013).