Predictive ability of problem-solving efficacy sources on mathematics achievement

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ABSTRACT
This study examined the relationship between mathematics achievement and mathematics problem-solving efficacy sources. A cluster sample of 123 first year prospective teachers of a Philippine higher education institution responded to a 30-item problem-solving efficacy scales and took the teacher-made tests in Mathematics in the Modern World course; namely, Non-Routine Problem Solving and Numbers and Patterns (NRPS-NNPT), Math Language and Symbols (MLS), and Data Management (DM). The research data was analyzed using Descriptive statistics, Pearson-r and Standard Multiple Regression. On the average, the respondents had satisfactory mathematics achievement. They reported a high level of social persuasion and somatic response and a low level of vicarious experience and mastery experience in mathematics problem-solving. Vicarious experience was directly associated with mastery experience while social persuasion and mastery experience were both inversely related to somatic responses. Among the four problem-solving efficacy sources, only social persuasion significantly predicted mathematics achievement specifically in the areas of NRPS-NNPT, MLS, and DM. Thus, becoming a trusted voice of encouragement and designing a persuasive and optimistic learning environment are highly recommended roles of schools to facilitate students' mathematics achievement.

Keywords:
Efficacy
Mastery experience
Mathematics achievement
social persuasion
Problem-solving
Vicarious experience

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1. INTRODUCTION
One of the most important competencies students must acquire today to increase their opportunities and potentials for success, is mathematical knowledge and skills [1]. Ironically, the achievements of typical students in college mathematics are not satisfactory, if not below the standards [2], [3]. Several investigations have established that affective characteristics are important factors that affect achievement [4]-[6] particularly, mathematics achievement [7]-[12]. One of these affective characteristics is self-efficacy belief [5], [7], [9], [10], [13], [14].

Self-efficacy comes from four main sources based on literature: mastery experience, vicarious experience, social persuasion, and somatic responses. Mastery experience is the result of one's previous experience that allows students to apply concepts they have already learned [12] and is the strongest source of self-efficacy [5]. Vicarious experience is seeing a role model who is doing the related task successfully and who has positive or negative effect on one's self-efficacy [13]. Social persuasion is mainly the feedback, negative or positive, to the performance of an individual from the people around [12]; and somatic responses
are basically the mood of the individual in performing and completing the task such that doing the task while experiencing stress and anxiety may result to incompetency and very low performance [5].

According to Bandura [5], self-efficacy beliefs pervasively influence people in achieving their goals, the amount of effort they apply in the task, and their perseverance in facing difficulties and stress. Mastery experiences, according to other studies, are also shown to be significantly related to some self-efficacy sources [15], [16]. Most studies show the variations on the level of significance of self-efficacy and mastery experiences [7], [12], [15], [16]. Similarly, several studies assert different levels of significance between psychological states and vicarious experiences [7], [17]-[19]. On the other hand, a study affirms that self-efficacy and vicarious experiences are insignificantly related [18].

Most studies assert that the strongest predictor of mathematics achievement is mastery experiences, followed by social persuasions, physiological states, and the weakest predictor is vicarious experiences [12], [19]-[21]. On the other hand, there are some studies that argue social persuasion has greater association with mathematics achievement than the three [17], [22], [23]; mathematics performance and vicarious experiences have no relationship [17], [22]; and the relationships of psychological states with academic achievement and mathematics achievement vary i.e. while some studies show that physiological states are significant factors of achievement [16], [17], [24], [25], others assert that it has low and insignificant effect [19], [24], [26]-[28].

Clearly, there are inconsistent results among studies that examined the relations between the four self-efficacy sources and between self-efficacy and mathematics achievement. The results vary depending on cultural differences and educational level [15], [16]. Most studies on these constructs have focused on self-efficacy and academic achievement among children and high school students abroad. Little is known today about the mathematics problem-solving efficacy and the mathematics achievement of Filipino prospective teachers particularly in Mathematics in the Modern World (MMW) course.

Mathematics problem-solving efficacy is a specific type of self-efficacy. It particularly refers to one’s perceived ability to solve a mathematical problem or task. Problem-solving efficacy is also determined by social persuasion, somatic responses, vicarious experiences, and mastery experiences [23]. Hence, the problem-solving efficacy of prospective teachers reflects their confidence in their ability to execute the skills necessary for learning their current mathematics course which is MMW.

MMW is a 3-unit general education course offered among first year students in the Philippines. As part of the CHED K-12 transition program for 2016-2021, the course deals with mathematics as an exploration of patterns, application of inductive and deductive reasoning, and a tool in daily life. In the current study, mathematics achievement refers to the test (percent) scores of the students in the three main lessons of MMW; namely, Non-Routine Problem-Solving and Nature and Number Patterns Tracing (NRPS & NNPT), Mathematical Language and Symbols (MLS), and Data Management (DM).

Hence, the current study aims to examine the relations between the problem-solving efficacy sources and the mathematics achievement of Filipino prospective teachers. Specifically, this study sought answers to the following questions: i) What is the mathematics achievement of the prospective teachers?; ii) What are their problem-solving efficacy sources?; iii) Is there a significant relationship between and among their mastery experiences, vicarious experiences, social persuasions, and somatic responses?; and iv) Which of the problem-solving efficacy sources can significantly predict mathematics achievement?

It is hoped that this study can further the understanding of the importance of self-efficacy on Filipino prospective teachers’ success in college mathematics, and provide important discussions with the abovementioned contradicting literature findings. As future teachers, their acquisition of mathematical competencies is highly important and their problem-solving efficacy might affect their mathematics achievement. Therefore, this study can help teacher educators especially mathematics teachers to integrate in the instructional planning and implementation the degree of importance of each problem-solving efficacy source on mathematics performance.

2. RESEARCH METHOD

2.1. Research design

This study utilized correlational design to assess the relationship between students’ mathematics achievements and problem-solving efficacy sources. According to Creswell [29], a correlational design is a non-experimental form of research that uses correlational statistics to describe and measure the degree of relationship between two or more quantitative variables.

2.2. Participants

The current study targets all education students enrolled in GEC 03: Mathematics in the Modern World (MMW) in a university during the school year 2019-2020. To control the effect of extraneous variables, a cluster sampling was done to select one higher education institution where students were taught...
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Problem-solving efficacy level was classified based on the summation of the four problem-solving efficacy source mean scores i.e., low efficacy for a sum of 11 or below while high efficacy for 12 or above. Data normalization using the technique introduced by Templeton [32] was conducted prior to regression analysis. The continuous variables were converted first as fractional ranks and then the fractional ranks were transformed into normalized continuous variables using idf.normal command of the SPSS. The normality test results after this data transformation technique is shown in Table 3.

### Table 3. Normality check

| Variables         | Kolmogorov-Smirnov* Statistic | df  | Sig.     | Shapiro-Wilk Statistic | DF  | Sig.     |
|-------------------|--------------------------------|-----|---------|------------------------|-----|---------|
| Normal_RPS        | .053                           | 120 | .200    | .994                   | 120 | .915    |
| Normal_Loogy      | .034                           | 120 | .200    | .995                   | 120 | .965    |
| Normal_Statistics | .045                           | 120 | .200    | .995                   | 120 | .955    |
| Normal_SocialPers | .059                           | 120 | .200    | .993                   | 120 | .775    |
| Normal_SomaticRes | .066                           | 120 | .200    | .991                   | 120 | .668    |
| Normal_Vicarious  | .054                           | 120 | .200    | .990                   | 120 | .492    |
| Normal_Mastery    | .064                           | 120 | .200    | .984                   | 120 | .172    |

Pearson’s correlational analysis was conducted to establish the relationship between efficacy sources and to check for multicollinearity i.e., variables that are highly correlated ($r > .80$). Multicollinearity check showed that the correlation coefficients were all less than .72; suggesting that the assumption was met [31], [33]. Hence, a Standard Multiple Regression analysis was conducted to explore which of the four problem-solving efficacy sources significantly affected mathematics achievements in NRPS & NNPT, MLS, and DM.

### RESULTS

Table 4 shows students’ achievement in mathematics. On the average, the students got 7 in every 10 merits in the mathematics tests. Thus, they had satisfactory achievements in the three mathematics areas. Table 5 shows their levels of self-efficacy sources. As can be gleaned on the table, they indicated that they have a high social persuasion and a somatic response level but they have a low vicarious experience and a mastery experience in mathematics problem-solving.

### Table 4. Students’ achievement in mathematics

| Area of mathematics  | M     | SD    | Description   |
|----------------------|-------|-------|---------------|
| NRPS and NNPT        | 66.40 | 16.360| Satisfactory  |
| MLS                  | 71.07 | 10.084| Satisfactory  |
| DM                   | 67.17 | 12.865| Satisfactory  |
| Overall              | 68.21 | 10.601| Satisfactory  |

### Table 5. Students’ levels of self-efficacy sources

| Dimensions          | No. of items | M     | SD    | Level |
|---------------------|--------------|-------|-------|-------|
| Social persuasion   | 10           | 35.34 | 6.33  | High  |
| Somatic responses   | 10           | 35.69 | 6.25  | High  |
| Vicarious experiences| 5            | 14.45 | 4.37  | Low   |
| Mastery experiences | 5            | 16.26 | 3.04  | Low   |
| Total efficacy      | 30           | 90.37 | 7.50  | Low   |

Table 6 shows the relationship between the four problem-solving efficacy sources. The results affirm that both social persuasion ($X_2$) and mastery experience ($X_4$) were both significantly associated with somatic responses ($X_1$). Social persuasions and mastery experiences significantly explained 50.69% and 3.84% of the variance in somatic responses, respectively. Moreover, vicarious experience ($X_3$) positively influences mastery experience ($X_4$), $r = .553$, $p < .01$ and shares 30.58% variance in mastery experience.

The results of the multiple regression analyses as shown in Table 7 indicate that among the four sources of problem-solving efficacy, only social persuasion significantly predicted the students’ mathematics achievement in NRPS & NNPT ($\beta = .378; p < .05$), MLS ($\beta = .464; p < .01$), DM ($\beta = .382; p < .01$), and their overall mathematics achievement ($\beta = .400; p < .01$).
TABLE 6. Multiple correlations of the problem-solving efficacy sources

| Variables               | X1   | X2   | X3   | X4   |
|-------------------------|------|------|------|------|
| Social persuasions (X1) | 1    | -.712* | .260* | .215* |
| Somatic responses (X2)  | 1    | -.151 | -.196* |       |
| Vicarious experiences   | 1    | .553* |       |       |
| Mastery experiences     | 1    |      |       |       |

**means significant at .01 level (two-tailed)
*means significant at .05 level (two-tailed)

4. DISCUSSION

This study aimed to assess the underlying construct of students’ problem-solving efficacy sources to determine the extent to which these sources significantly predict mathematics achievement. Results indicated that social persuasions and mastery experiences negatively associate with somatic responses. Meaning, as social persuasion (or mastery experience) increases, somatic responses decreases. Social persuasion explains around 51% (while mastery experience explains around 4%) of the variance in somatic responses. Vicarious experiences and mastery experiences are positively correlated and share 30.58% of their variance. These patterns of relationships between the four self-efficacy sources do not agree to some extent with previous research. For instance, Capa-Aydin, Kondakci, and Ceylandag [34] argue that mastery experiences have a mediation effect for social persuasion and physiological state but no mediation effect for vicarious experiences. Usher and Pajares [18] assert that vicarious experience is not significantly associated with self-efficacy. Similarly, the result of the current study rebuts the finding of several researches [7], [17]-[19] that vicarious experience is significantly related to somatic response.

Among the four efficacy sources, only social persuasions achieved significant results in explaining achievements in mathematics in the areas of solving non-routine problems and tracing patterns in nature and numbers, logic, and statistics (with beta ranging from .378 to .47). It agrees with studies [17], [22] that the strongest efficacy source predictor of mathematics achievement is praise and feedback. On the other hand, it refutes the claim of previous studies [5], [12], [19], [21] that mastery experience is the best predictor of mathematics performance. The result of the current study also neglects the assertion of several researches [16], [17], [24], [25] that stated somatic response is a significant factor of academic achievement. On the other hand, it affirms the statement of several studies [19], [24], [26]-[28] that somatic response has a low and insignificant effect. Moreover, the current finding highlights that vicarious experience as a mathematics problem-solving efficacy source does not significantly contribute to mathematics achievement [7], [17], [22].

5. CONCLUSION

This quantitative research found that social persuasions and mastery experiences are both inversely associated with somatic responses, and among the four efficacy sources indicated in the literature, only social persuasions can significantly predict mathematics achievement in the areas of solving non-routine problems and tracing patterns in nature and numbers, logic, and statistics.

This study contributes to the understanding of the roles of the four mathematics problem-solving efficacy sources on mathematics achievement and guides the decision of schools as to which of the sources should be given more attention and priority to better enhance students’ performance in mathematics. The study suggests that maintaining an encouraging learning environment and expanding students’ mastery learning opportunities could reduce students’ anxiety in solving mathematics problems or tasks. The significance of the predictive ability of social persuasion on mathematics achievement supports that
becoming a trusted voice of encouragement and designing a persuasive learning environment are highly recommended roles of schools in facilitating the students to attain the necessary competencies of the course. Mathematics teachers should give sincere and timely feedback to students’ progress toward a learning goal and encourage them to attribute success and failure in mathematics to the amount of effort they exerted in learning. Nevertheless, the students should be enabled to evaluate their own learning progress against the desired mathematical competencies and outcomes rather than against the learning performance of other students.

However, the variations of the findings with existing studies might be due to the distinct nature of the tests administered to the students and the areas of mathematics involved. Both the NRPS & NNPT and the DM tests contained multiple-choice type while the MLS test focused on mathematical logic (which cannot be measured validly by multiple-choice). The reliability index of these tests was not established. The study was also limited to a linear regression model between mathematics problem-solving efficacy sources and mathematics achievement.

Future research may wish to replicate the current study using standardized measuring instruments. Other affective variables such as attitude toward mathematics, mathematics anxiety, and motivation may be included through a structural equation model to get a more holistic and realistic measure of the relationship of these variables on mathematics achievement. A qualitative research may be conducted to understand how social persuasion enhances the learning of mathematics and to explore the phenomenology of teachers’ engagement in giving feedback and praise in their classroom.

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