Charged meson rapidity distributions in central Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV

I. G. Bearden$^7$, D. Beavis$^1$, C. Beslin$^{10}$, B. Budick$^6$, H. Bøggild$^7$, C. Chasman$^1$, C. H. Christensen$^7$, P. Christiansen$^7$, J. Cibor$^3$, R. Debbe$^3$, E. Enger$^{12}$, J. J. Gaardhøje$^7$, M. Germinario$^7$, K. Hagel$^8$, O. Hansen$^7$, A. Holm$^7$, A. K. Holme$^{12}$, H. Ito$^{11}$, A. Jipa$^{10}$, F. Jung$^2$, J. I. Jørdre$^9$, C. E. Jørgensen$^7$, R. Karabowicz$^4$, E. J. Kim$^{11}$, T. Kozik$^4$, T. M. Larsen$^{12}$, J. H. Lee$^1$, Y. K. Lee$^5$, G. Levhøiden$^{12}$, Z. Majka$^4$, A. Makeev$^8$, M. Mikelsen$^{12}$, M. Murray$^{11}$, J. Natowitz$^9$, B. S. Nielsen$^7$, J. Norris$^{11}$, K. Olchanski$^1$, D. Ouerdane$^7$, R. Planeta$^4$, F. Ramí$^2$, C. Ristea$^{10}$, D. Röhrich$^9$, B. H. Samset$^{12}$, D. Sandberg$^7$, S. J. Sanders$^{11}$, R. A. Sheetz$^1$, P. Stasz$^7$, T. S. Tvet$^{12}$, F. Videbaek$^1$, R. Wada$^8$, Z. Yin$^9$, and I. S. Zgura$^{10}$

(BRAHMS Collaboration)

1 Brookhaven National Laboratory, Upton, New York 11973,
2 Institut de Recherches Subatomiques and Université Louis Pasteur, Strasbourg, France,
3 Institute of Nuclear Physics, Krakow, Poland,
4 Jagiellonian University, Krakow, Poland,
5 Johns Hopkins University, Baltimore, Maryland 21218,
6 New York University, New York, New York 10003,
7 Niels Bohr Institute, University of Copenhagen, Denmark,
8 Texas A&M University, College Station, Texas 77843,
9 University of Bergen, Department of Physics, Bergen, Norway,
10 University of Bucharest, Romania,
11 University of Kansas, Lawrence, Kansas 66049,
12 University of Oslo, Department of Physics, Oslo, Norway

We have measured rapidity densities $dN/dy$ of $\pi^\pm$ and $K^\pm$ over a broad rapidity range ($-0.1 < y < 3.5$) for central Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV. These data have significant implications for the chemistry and dynamics of the dense system that is initially created in the collisions. The full phase-space yields are $1660 \pm 90$ for the 5% most central Au+Au collisions and $242 \pm 4 \pm 19 (K^-)$. The systematics of the strange to non-strange meson ratios are found to track the variation of the baryo-chemical potential with rapidity and energy. Landau–Carruthers hydrodynamic is found to describe the bulk transport of the pions in the longitudinal direction.

In ultra-relativistic heavy ion collisions at RHIC energies, charged pions and kaons are produced copiously. The yields of these light mesons are indicators of the entropy and strangeness created in the reactions, sensitive observables to the possible existence of an early color deconfined phase, the so-called quark gluon plasma. In such collisions, the large number of produced particles and their subsequent reinteractions, either at the partonic or hadronic level, motivate the application of concepts of gas or fluid dynamics in their interpretation. Hydrodynamical properties of the expanding matter created in heavy ion reactions have been discussed by Landau [1] (full stopping) and Bjorken [2] (transparency), in theoretical pictures using different initial conditions. In both scenarios, thermal equilibrium is quickly achieved and the subsequent isentropic expansion is governed by hydrodynamics. The relative abundances and kinematic properties of particles provide an important tool for testing whether equilibrium occurs in the course of the collision. In discussing the source characteristics, it is important to measure most of the produced particles in order not to violate conservation laws (e.g. strangeness and charge conservation).

In this letter, we report on the first measurements at RHIC energies of transverse momentum ($p_T$) spectra of $\pi^\pm$ and $K^\pm$ over the rapidity range $-0.1 < y < 3.5$ for the 5% most central Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV. The spectra are integrated to obtain yields as a function of rapidity ($dN/dy$), giving full phase-space (4$\pi$) yields. At RHIC energies, a low net-baryon density is observed at mid-rapidity $y$, so mesons may be predominantly produced from the decay of the strong color field created initially. At forward rapidities, where primordial baryons are more abundant $\xi$, other production mechanisms, for example associated strangeness production, play a larger role. Therefore, the observed rapidity distributions provide a sensitive test of models describing the space-time evolution of the reaction, such as Landau and Bjorken models [1, 2]. In addition, integrated yields are a key input to statistical models of particle production $\xi$.

BRAHMS consists of two hadron spectrometers, a mid-rapidity arm (MRS) and a forward rapidity arm (FS), as well as a set of detectors for global event characterization $\xi$. Collision centrality is determined from charged particle multiplicities, measured by scintillator tile and silicon multiplicity arrays located around the nominal interaction point. The interaction vertex is measured with a resolution of 0.6 cm by arrays of Čerenkov
counters positioned on either side of the nominal vertex. Particle identification (PID) for momenta below 2 GeV/c is performed via time–of–flight (TOF) in the MRS. In the FS, TOF capabilities allow π–K separation up to $p = 4.5$ GeV/c, and is further extended up to 20 GeV/c using a ring imaging Čerenkov detector. Further details can be found in [7, 8].

Further details are not necessary for the current context.

Figure 1 shows transverse mass $m_T - m_0$ spectra ($m_T = \sqrt{p_T^2 + m_0^2}$) for $\pi^-$ and $K^-$. Particle spectra were obtained by combining data from several spectrometer settings (magnetic field and angle), each of which covers a small region of the phase–space ($y, p_T$). The data have been corrected for the limited acceptance of the spectrometers using a Monte-Carlo calculation simulating the geometry and tracking of the BRAHMS detector system. Detector efficiency, multiple scattering and in-flight decay corrections have been estimated using the same technique. Hyperon ($\Lambda$) and neutral kaon $K_{0s}$ decays may have contaminated the pion sample. For $K_{0s}$, it is assumed that its yields amount to the average between $K^+$ and $K^-$ at each rapidity interval. For $\Lambda$ yields, since only mid–rapidity data are available, we used the same assumptions as in [2], namely $\Lambda/p = \Lambda/\bar{p} = 0.9$ in the phase–space covered in this analysis. The fraction of pions originating from $\Lambda$ and $K_{0s}$ decays was estimated with a GEANT simulation where realistic particle distributions (following an exponential in $m_T$) were generated for several spectrometer settings. Particles were tracked through the spectrometers and produced pions were accepted according to the same data cuts applied to the experimental data. It has been found a $K_{0s}$ ($\Lambda$) contamination of 4% ($\lesssim 1\%$) in the MRS and 6% ($\lesssim 1\%$) in the forward spectrometer. In the following, the pion yields are corrected unless stated otherwise.

The pion spectra are well described at all rapidities by a power law in $p_T$, $A(1 + p_T/p_0)^{-n}$. For kaons, an exponential in $m_T - m_0$, $A \exp \left(\frac{m_T - m_0}{\Gamma}\right)$, has been used. The invariant yields $dN/dy$ were calculated by integrating the fit functions over the full $p_T$ or $m_T$ range. The two main sources of systematic error on $dN/dy$ and $\langle p_T \rangle$ are the extrapolation in the low $p_T$ range outside the acceptance, and the normalization of the spectra. Other fit functions were used in order to estimate the error on the extrapolation. In the FS, due to a smaller acceptance coverage at low $p_T$, the error is systematically larger than in the MRS. In total, the systematic error amounts to $\sim 10\%$ in the range $-0.1 < y < 1.4$ (MRS) and $\sim 15\%$ for $y > 2$ (FS). Mid–rapidity yields recently reported by the STAR [9] and PHENIX experiments [10] are within 1 $\sigma_{\text{sys}}$ of these results.

Rapidity densities and mean transverse momenta $\langle p_T \rangle$ extracted from the fits are shown in Fig. 2. Panel (a) shows the pion and kaon rapidity densities (a) and their mean transverse momentum $\langle p_T \rangle$ (b) as a function of rapidity. Errors are statistical. The kaon yields were multiplied by 4 for clarity. The dashed lines in (a) are Gaussian fits to the $dN/dy$ distributions (see text).
and \(K^\pm\) we have investigated several fit functions: a single Gaussian centered at \(y = 0\) (G1), a sum of two Gaussians (G2) or Woods-Saxon (WS) distributions placed symmetrically around \(y = 0\). Our data do not distinguish among these functions, all give a \(\chi^2\) per d.o.f. of \(\sim 1\), and have the same total integral to within 2\% (cf. Tab. I).

| \(\pi^+\) | \(\pi\) | \(K^+\) | \(K^0\) |
|---|---|---|---|
| WS | 1677 ± 17 | 1695 ± 15 | 293 ± 6 | 243 ± 2 |
| G1 | 1660 ± 15 | 1683 ± 16 | 286 ± 5 | 242 ± 4 |
| G2 | 1640 ± 16 | 1655 ± 15 | 285 ± 5 | 239 ± 3 |

TABLE I: Full phase–space yields of \(\pi^\pm\) and \(K^\pm\) extracted from fits to the \(dN/dy\) distributions (see text). Errors are statistical, systematic errors are of the order of 8\%.

Figure 3(a) shows ratios of the strange to non–strange full phase–space meson yields \((K/\pi)\) as a function of \(\sqrt{s_{NN}}\). The ratio \(K^+ / \pi^+\) shows a fast increase from low AGS to low SPS energies (\(\sqrt{s_{NN}} = 8\) GeV), followed by a decrease with increasing energy. At \(\sqrt{s_{NN}} = 200\) GeV, we find a value of \(0.173 \pm 0.003 \pm 0.014\), consistent with the ratio at the highest SPS energy. In contrast, \(K^- / \pi^-\) increases monotonically but remains below \(K^+ / \pi^+\). At \(\sqrt{s_{NN}} = 200\) GeV, it reaches a value of \(0.143 \pm 0.003 \pm 0.011\), a value close to the positive ratio. It is interesting to compare the energy systematic with the rapidity dependence at \(\sqrt{s_{NN}} = 200\) GeV (Fig. 3(b)). A fit to a straight line in the range \(0 < y < 1.3\) gives \(K^+ / \pi^+ = 0.162 \pm 0.001\) (stat) and \(K^- / \pi^- = 0.154 \pm 0.001\). The dashed and dotted lines are predictions of the hadron gas statistical model [28], where a chemical freeze–out temperature \(T = 177\) MeV and baryo–chemical potential \(\mu_B = 29\) MeV were used (the authors used a fit to particle ratios at \(\sqrt{s_{NN}} = 130\) GeV in the rapidity range \(|y| < 0.5\) for extrapolating mid–rapidity ratios at the top RHIC energy). The agreement with the data is consistent within the systematic errors [22]. However, the data deviate from the model prediction at \(y > 2\), where an increasing excess of \(K^+\) over \(K^-\) is observed. This may be due to an increase of the net–baryon densities [2, 4]. A baryon rich environment is favorable for associated strangeness production, e.g. \(p + p \rightarrow p + K^+ + \Lambda\), a production channel forbidden to \(K^-\). In the context of the statistical model, this translates into an increase of the baryo–chemical potential \(\mu_B\), as already reported in [3], where a calculation by Becattini et al. [3] of \(K^+ / K^-\) vs \(p/p\) at constant \(T\) (and varying \(\mu_B\)) agrees well with the rapidity dependence of the experimental ratios.

The observed rapidity distributions of pions exhibit a nearly Gaussian shape. Widths are found to be \(\sigma_{\pi^+} = 2.25 \pm 0.02\) (stat) and \(\sigma_{\pi^-} = 2.29 \pm 0.02\) rapidity units. Similar overall features have already been observed in central Au+Au collisions at AGS [17] and Pb+Pb reactions at SPS [16]. This is reminiscent of the hydrodynamical expansion model proposed by Landau [1]. In the initial state, colliding nuclei are highly Lorentz contracted along the beam direction. Under assumptions of full stopping and isentropic expansion after the initial compression phase (where thermal equilibrium is reached), the hydrodynamical equations (using the equation of state of a relativistic gas of massless particles) lead to \(dN/dy\) distributions of Gaussian shape at freeze–out [15]. The original Landau model was simplified and used by Carruthers et al. for the description of particle production in p+p collisions [13, 20, 21]. In their model, the width \(\sigma\) of the pion distribution is simply formulated:

\[
\sigma^2 = \ln \gamma_{\text{beam}} = \ln \left(\sqrt{s} / 2m_p\right)
\]

where \(m_p\) is the proton mass. To extend this formula to heavy ion collisions, one might naively replace \(\sqrt{s}\) by \(\sqrt{s_{NN}}\). Figure 4(a) shows the experimental \(dN/dy(\pi)\) and Carruthers Gaussians at \(\sqrt{s_{NN}} = 200\) GeV (using Eq. 1 with the condition that the integrals of these Gaussians must be equal to the full–space yields extracted from the data). Surprisingly, a discrepancy of only \(\sim 5\%\) between the model and the data is observed (\(\sigma_{\text{Carrut.}} = 2.16\). The inset in Fig. 4 shows the ratio \(\sigma_{\text{data}} / \sigma_{\text{Carrut.}}\) as a function of \(\sqrt{s_{NN}}\). At all energies, the widths \(\sigma_{\text{data}}\) result from Gaussian fits to the pion distributions. While the difference between theory and measurements is of the order of 10\% at most from AGS to RHIC energies, it is worth noting that the overall systematic may not be trivial. The ratio at RHIC is \(~ 15\%\) higher than at SPS. It is furthermore interesting to note that in central Au+Au collisions at \(\sqrt{s_{NN}} = 200\) GeV, the original baryons lose 2 rapidity units on average from the initial value \(y_b = 5.36\) [3]. Not only is the degree of transparency significantly different between AGS and RHIC, but the relative rapidity loss \(\langle \delta y \rangle / y_b\) is about half lower [3].

On the basis of the Landau’s original hydrodynamic, Bjorken [2] proposed a scenario in which yields of produced particles would be boost–invariant within a region around mid–rapidity. In that approach, reactions are described as highly transparent leading to a vanishing net–baryon density around mid-rapidity and particle production from pair creation from the color field in the central zone. This would result in a flat distribution of particle yields around \(y = 0\). As mentioned, collisions at RHIC are neither fully stopped nor fully transparent, although a significant degree of transparency is observed. Consequently the overall \(dN/dy\) distribution of pions is expected to consist of the sum of the particles produced in the boost invariant central zone and the particles produced by the excited fragments. The fact that the observed distributions are flatter at mid-rapidity and wider than those predicted by the Landau–Carruthers model might point in this direction.

In summary, we have measured transverse momentum
spectra and inclusive invariant yields of charged meson $\pi^\pm$ and $K^\pm$. The ratios to non–strange mesons $K/\pi$ are well reproduced by the hadron gas statistical model [6] that assumes strangeness equilibrium at mid–rapidity. The excess of $K^+$ over $K^-$ yields at higher rapidities can be explained by the increasing baryo–chemical potential $\mu_B$ with rapidity. The widths of the pion rapidity distributions are in surprisingly good agreement with a hydrodynamic model based on the Landau expansion picture.

This work was supported by the division of Nuclear Physics of the Office of Science of the U.S. DOE, the Danish Natural Science Research Council, the Research Council of Norway, the Polish State Com. for Scientific Research and the Romanian Ministry of Research.

[1] L. D. Landau, Izv. Akad. Nauk SSSR Ser. Fiz. 17, 51 (1953).
[2] J. D. Bjorken, Phys. Rev. D27, 140 (1983).
[3] I. G. Bearden et al. (BRAHMS) (2003), nucl-ex/0312023.
[4] I. G. Bearden et al. (BRAHMS), Phys. Rev. Lett. 90, 102301 (2003).
[5] F. Becattini, J. Cleymans, A. Keranen, E. Suhonen, and K. Redlich, Phys. Rev. C64, 024901 (2001).
[6] P. Braun-Munzinger, D. Magesto, K. Redlich, and J. Stachel, Phys. Lett. B518, 41 (2001).
[7] M. Adamczyk et al. (BRAHMS), Nucl. Instrum. Meth. A499, 437 (2003).
[8] D. Ouerdane, Ph.D. thesis, University of Copenhagen (2003).
[9] J. Adams et al. (STAR), Phys. Rev.Lett. 92, 112301 (2004), nucl-ex/0310004.
[10] S. S. Adler et al. (PHENIX), Phys. Rev. C69, 034909 (2004).
[11] BRAHMS, URL http://www4.rcf.bnl.gov/brahms/WWW/publications.html.
[12] L. Ahle et al. (E802), Phys. Rev. C57, 466 (1998).
[13] L. Ahle et al. (E866 and E917), Phys. Lett. B476, 1 (2000).
It should be noted that the $\Lambda$ and $K_0s$ feed down correction applied to the data is significantly different from the amount of feed down assumed in the model calculations. When not corrected for particle feed down, the data show excellent agreement with the model prediction.