Design and Fatigue Optimization of Drive Shaft

Ashish Bawkar¹, Tejas Ambekar², Prathamash Amle³, Tejas Bhosale⁴, Prof. Ashish Mujumdar⁵
¹, ², ³, ⁴Students, Mechanical Engineering, Vishwakarma Institute of Technology, Pune, India
⁵Faculty, Mechanical Engineering, Vishwakarma Institute of Technology, Pune, India

Abstract: This work aims towards the design and optimization of the drive shaft as there is increasing demand for weight reduction in an automobile vehicle. The drive shaft is basically a torque transmitting element which transmit the torque from the differential gearbox to the respective wheels. In general, the drive shafts are subjected to fluctuating loads as the torque requirement changes according to the road conditions. Due to this, the drive shaft should be designed considering fatigue failure. The Maruti Suzuki Ertiga model is chosen for design and optimization of the drive shaft. For the fatigue life prediction of the drive shaft, the S-N curve approach is used. Furthermore, the inner diameter of the shaft is varied to obtain the optimized diameter of a hollow shaft which can withstand these fluctuating loads without failure. Along with fatigue life prediction, the natural frequency of the hollow shaft is also calculated. Furthermore, the parametric analysis is carried out of fatigue FOS, Von mises stress, weight and natural frequency of the shaft by varying the diameter ratio of the hollow shaft, and the nature of variation of these parameters are plotted in their respective graphs. The design is validated by performing FEA analysis for each case of a hollow shaft using Ansys software. Finally, from the FEA analysis we conclude that the optimized dimensions of the hollow drive shaft are safe.

Keywords: Drive Shaft, Optimization, Fatigue Failure, S-N curve, Fatigue analysis, FEA.

I. INTRODUCTION

The drive shaft is a mechanical component or part which transmits torque to the respective wheels from a differential gearbox. In simple words, it is a torque transmitting element, its function is to drive the vehicle. It can also be used to transmits torque at varying angles between driveline components by implementing constant velocity joints or universal joints, etc. Basically, the materials that are used in the drive shaft are ANSI-AISI 1340-50, 3140-50, 4140, 4340, 4820 and 8620. Here, the material chosen is AISI 4340-oil quenched which is having mechanical property Density=7.85 g/cc, Ultimate Tensile Strength-1985 MPa, Yield Strength-1840 MPa, Poisson’s Ratio-0.30, and Shear Modulus-81.5 GPa.

Fig.1 Drive shaft

For Fatigue life prediction we have S-N curves, E-N curve and Fracture mechanic’s approach. The S-N curve is plotted between nominal stress amplitude (S) vs Cycles of Failure (N). From this, if the applied stress level is below the endurance limit of the material, the elements or components are said to have an infinite life. The S-N curve approach is basically used for high-cycle fatigue problems. In case of the E-N curve, we get to know that when strains are no longer elastic, such as in the presence of stress concentrations, the total strain can be used instead of stress as a similitude parameter. The E-N curve approach is used for the Low Cycle fatigue problems. The Fracture mechanics approach is for the propagation of cracks in material to characterize the material’s resistance to failure. It is used to predict the failure of the component with an exciting crack. Fatigue Failure criterion includes the Soderberg, Goodman, Gerber line and other approaches. For this project we used the Modified Goodman Criterion because it is a straight line joining (Se) on the ordinate to (Sut) on the abscissa, and the straight-line equations are linear and easy. So, it can be easily plotted, and the time for computing and plotting will be saved. It reveals subtleties insight into fatigue problems, and answers can be easily scaled from the graph.
The whirling of the drive shaft can be expressed as when the drive shaft rotates at speed equal to the natural frequency of transverse oscillations, this causes vibrations in shaft which is eventually called whirling of the drive shaft. Natural frequency is the frequency at which a system tends to oscillate in the absence of damping force, and when the natural frequency gets equal to forced frequency, then resonance occurs. This resonance frequency will fail the drive shaft more quickly.

Fig. 2 Whirling of shaft

The drive shaft is assumed that the drive shaft is simply supported and free to rotate normal to the axis. The first mode of natural frequency is taken into account for the calculation. The above figure shows the shape of deflection for the first mode of natural frequency.

II. LITERATURE SURVEY

Shafts are designed by the applied torsional loads and selecting inner and outer diameters not to exceed the material's yield strength. Different combinations of inner and outer diameters will support the loads, and the final dimensions may be chosen based on the designer's attempt to minimize both mass and rotational inertia. [2] Fatigue was the dominant mechanism of drive shaft failure due to benchmarks on the cracked surfaces. Fatigue cracks initiated from the root fillet region of the spline gear. [3] The endurance limit correction factors, fatigue strength of the material and fatigue life of the component are considered to create a stress-cycle (S-N) diagram that is sustained by the shaft before damaged. [4] The Finite element analysis was carried out with full torsional load on a 3-D model of composite propeller shaft for torque bearing capacity, stiffness, bending natural frequency. [5] The weight reduction of the drive shaft can have a certain role in the weight reduction of the vehicle and is a highly recommended, desirable goal if it can be achieved with same cost and performance. It is possible to reduce the weight of the drive shaft considerably by optimizing the design parameters by satisfying all the constraints. [6] Factor of safety plays an important role during fatigue analysis. As the drive shaft is a critical part of a vehicle, it makes the designer to consider the higher factor of safety for application in the range of 2.7 to 12.8, but most of the time refers to the factor of safety as 3 to 4. The main objective of the paper is to design a hollow drive shaft which is having same performance as that of a solid shaft with the advantage of weight reduction. Furthermore, the parametric analysis is carried out to study the nature of variation of the Fatigue FOS, Von Mises stress, weight and natural frequency of the drive shaft when diameter ratio is varied. Also, effort is made to analyse the designed shaft for structural and fatigue failure using static structure analysis and to analyse the critical speed of the drive shaft using modal analysis.

III. DESIGN CALCULATIONS

A. Torque calculations

We have selected Maruti Suzuki Ertiga for drive shaft calculations. The following are the specifications of it.

| TABLE I SPECIFICATIONS |
|-------------------------|
| Engine Torque $T_e$ (Nm.) | 138 |
| 1 Gear Ratio $i_1$ | 2.875 |
| Final Drive Ratio $i_f$ | 4.375 |

Maximum Torque at Drive shaft ($T_{max}$) = $(T_e * i_1 * i_f) / 2 = 867890.63$ N.mm

B. Design of Solid Shaft

The drive shaft is subjected to pure torsional shear stress; therefore, we have $\tau = \frac{16 * T_{max}}{\pi * d^3}$

According to maximum shear stress theory of failure, we have $\tau = \frac{0.5 * S_{yt}}{FOS} = \frac{0.5 * 1840}{4} = 230$ MPa

Therefore, the required diameter of drive shaft is given by, $d = \sqrt[3]{\frac{16 * T_{max}}{\pi * \tau}} = 27$ mm

Weight of the drive shaft is given by, $W = \rho * \frac{\pi}{4} * d^2 * l$

$W = 7.85 * 10^{-6} * \frac{\pi}{4} * 27^2 * 240 = 1.08$ Kg
C. Calculation of Modified endurance limit of drive shaft

Modified endurance limit \( Se = K_a \times K_b \times K_c \times K_d \times K_e \times Se' \)

Endurance limit \( Se' = 0.5 \times S_{ut} = 992.5 \text{ MPa} \)

Surface finish factor \( K_a = a \times S_{ut}^b = 4.51 \times 1985^{-0.265} = 0.6 \)

Size factor \( K_b = 1.24 \times d^{-0.107} = 1.24 \times 27^{-0.107} = 0.88 \)

Loading Factor \( K_c = 0.59 \)

Temperature Factor \( K_d = \frac{S_T}{S_{RT}} = \frac{1010}{1008} = 1 \)

Reliability Factor \( K_e = 99\% = 0.814 \)

Modified endurance limit \( Se = 251.675 \text{ MPa} \)

Factor of safety using Modified Goodman Criteria,
\[
\sigma_m = \frac{\sigma_{max} - \sigma_{min}}{2}, \quad \sigma_a = \frac{\sigma_{max} + \sigma_{min}}{2}, \quad n = \frac{1}{3e + \frac{S_{ut}}{Se'}}
\]

D. Optimization of hollow shaft

The torsional shear stress induced in the hollow drive shaft is given by,
\[
\tau = \frac{16 \times T \times a}{\pi \times d_{o} \times (1 - C^4)}
\]

Here, \( C \) is the ratio of inside to outside diameter of hollow shaft.

Weight of the drive hollow shaft is given by,
\[
W = \rho \times \frac{\pi}{4} \times (d_{o}^2 - d_{i}^2) \times L
\]

Whirling of shaft, it is assumed that the drive shaft is simply supported and free to rotate normal to the axis.
\[
f = \frac{\pi}{2} \times n^2 \times \sqrt{\frac{gE}{\rho L^4}}
\]
\[
w = \rho \times A \times L
\]

As the value of \( C \) changes, the shear stress induced in the hollow shaft also changes, which will affect the fatigue factor of safety. Thus, maintaining the outer diameter constant, i.e., 27 mm and varying the \( C \) ratio, we get different inner diameter values as follows.

| TABLE III |
| OPTIMIZATION TABLE |

| C ratio | Outer diameter do (mm) | Inner diameter di (mm) | Torsional shear Stress \( \tau \) (MPa) | Goodman FOS n | Weight of Shaft W (kg) | Natural Frequency (Hz) |
|---------|---------------------|---------------------|-------------------------------|----------------|---------------------|----------------------|
| 0.1     | 27                  | 2.7                 | 224.59                        | 1.12           | 1.07                | 2054.50              |
| 0.2     | 27                  | 5.4                 | 224.93                        | 1.12           | 1.04                | 2084.79              |
| 0.3     | 27                  | 8.1                 | 226.40                        | 1.11           | 0.98                | 2134.31              |
| 0.4     | 27                  | 10.8                | 230.47                        | 1.09           | 0.91                | 2201.78              |
| 0.5     | 27                  | 13.5                | 239.54                        | 1.05           | 0.81                | 2285.60              |
| 0.56    | 27                  | 15.1                | 249.06                        | 1.01           | 0.74                | 2343.02              |

Thus, form the above table the safe dimensions of the drive shaft are \( do = 27 \text{ mm} \) and \( di = 15.1 \text{ mm} \), exceeding the diameter ratio \( C \) above 0.56 will result in fatigue failure of the drive shaft.
E. Calculations for SN Curve

Fatigue strength co-efficient $\sigma'f = S_{ut} + 345 = 2330$ MPa

$$b = \frac{-\log\left(\frac{\sigma'}{S_{ut}}\right)}{\log(2 + Ne)} = -0.0588$$

Fatigue strength factor $f = \frac{\sigma_{T}}{S_{ut}} \times (2 \times 1000)^b = 0.75064$

Alternating stress induced is given by, $S_{f} = aN^b$

Where a and b values are:

| TABLE III | S-N CURVE TABLE |
|-----------|-----------------|
| Low cycle fatigue region | High cycle fatigue region |
| $a = S_{ut} = 1985$ MPa | $a = \frac{(f \times S_{ut})^2}{S_{ce}} = 8821.36$ MPa |
| $b = \frac{\log(f)}{3} = -0.0415$ | $b = -\frac{1}{3} \log \left(\frac{S_{ut}}{S_{ce}}\right) = 0.2574$ |

From the above equation of low cycle and high cycle fatigue we plotted SN curve for the drive shaft.

![Fig. 3 S-N curve of drive shaft](image)

IV. RESULTS

A. Ansys Results

Static structure module is used to carry out Structural and fatigue analysis, the boundary conditions that are applied to the drive shaft are, one end of the shaft is fixed and the other end of the shaft is subjected to torsional moment. The modal module is used to carry out natural frequency analysis, the boundary condition that is applied to the drive shaft is both the ends of the shaft are fixed. Depending on these conditions, the FEA analysis is carried out, and the following results are obtained for each case.

![Fig. 4.1 Von mises Stress for C = 0.1](image)  ![Fig. 4.2 Von mises Stress for C = 0.2](image)
Fig. 5.3 Fatigue FOS For C = 0.3

Fig. 5.4 Fatigue FOS For C = 0.4

Fig. 5.5 Fatigue FOS For C = 0.5

Fig. 5.6 Fatigue FOS For C = 0.56

Fig. 5 Fatigue FOS
Fig. 6.1 Natural Frequency for C = 0.1

Fig. 6.2 Natural Frequency for C = 0.2

Fig. 6.3 Natural Frequency for C = 0.3

Fig. 6.4 Natural Frequency for C = 0.4

Fig. 6.5 Natural Frequency for C = 0.5
B. Validation
The von mises stress for shaft subjected to pure torsion is given by,

\[ \sigma_v = \sqrt{3} \tau \]

| Diameter Ratio C | Von Mises stress Analytical Result (MPa) | FEA Result (MPa) | Fatigue FOS Analytical Result | FEA Result | Whirling of shaft Analytical Result (Hz) | FEA Result (Hz) |
|------------------|----------------------------------------|-----------------|-------------------------------|------------|----------------------------------------|-----------------|
| 0.1              | 389.00                                  | 390.64          | 1.12                          | 1.14       | 2054.50                                | 2060.5          |
| 0.2              | 389.58                                  | 390.89          | 1.12                          | 1.14       | 2075.37                                | 2079.8          |
| 0.3              | 392.14                                  | 393.34          | 1.11                          | 1.13       | 2105.79                                | 2111.7          |
| 0.4              | 399.18                                  | 400.1           | 1.09                          | 1.12       | 2153.38                                | 2155.1          |
| 0.5              | 414.89                                  | 416.43          | 1.05                          | 1.07       | 2206.76                                | 2209.1          |
| 0.56             | 431.38                                  | 432.54          | 1.01                          | 1.03       | 2243.27                                | 2245.2          |

From the above tables we can conclude that the analytical result and FEA result have an error less than 1%. Thus, we conclude that the FEA analysis is correct.

V. DISCUSSION

![Graph between Von mises Stress Vs Diameter ratio](image_url)
From graph 1 we can conclude that, as the diameter ratio increases, the Von Mises stress induced in the shaft also increases. This is because the thickness of the hollow shaft decreases. From graph 2 we can conclude that, as the diameter ratio increases, the mass of the hollow shaft decreases. This is because the thickness of the shaft decreases. From graph 3 we can conclude that, as the diameter ratio increases, fatigue factor of safety decreases. This is because the amplitude of stress induced in the hollow shaft increases. From graph 4 we can conclude that, as the diameter ratio increases, the natural frequency of the shaft increases. This is because the mass of the hollow shaft decreases.
VI. CONCLUSION

The drive shaft is optimized and the final safe dimensions of the drive shaft for the given torque are outer diameter 27 mm and inner diameter 15.1 mm. The weight of the drive shaft is reduced by 68.52% when compared to the solid drive shaft. Also, the parametric analysis is carried out for the hollow shaft to study the nature of variation of the Fatigue FOS, Von Mises stress, weight and natural frequency of the drive shaft when diameter ratio is varied. Furthermore, the design of the drive shaft is validated using a FEA software Ansys. The results obtained from Ansys and the analytical method have an error less than 1%. This concludes that the optimized design of the drive shaft is safe.

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