Experimental investigation of proppant clustering in intersected fractures

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Abstract
This paper investigates the dynamics of proppant agglomerations during flow and transport within fractures intersected at the angles typical for the joint of pre-existing and newly formed fractures. The study considers variations and coupling of fluid flow rates, proppant volumetric concentrations, fluid dynamic viscosities and fracture intersection angles. Proppants are widely used during hydraulic fracturing to keep fractures open and enhance reservoir permeability. This study uses plexiglas experimental slots and visual analysis for identifying particle displacements. Geo-Particle Image Velocimetry–Reliability-Guided (GeoPIV-RG) method tracks particle movements among images by comparing the reference and subsequent snapshots at the point and time of interest. Results of this study show that the proppant volumetric concentration and the fluid flow rate are closely correlated with each other for affecting proppant flow, transport, and agglomeration formation. Increasing the proppant volumetric concentration generally promotes particle agglomeration, with different extent when coupled with the fluid flow rate. Proppant volumetric concentration affects the size, shape, and distribution of particle clusters. Increasing the fluid flow rate increases the occurrence of particle agglomerates at low proppant volumetric concentration; however, this trend is absent under high proppant volumetric concentrations. Sizes and shapes of proppant agglomerates change as the fluid flow rate changes. Changes of fracture intersection angle minimally affect shape, size and distance between proppant agglomerates and clusters. Furthermore, increasing the fluid dynamic viscosity strongly promotes proppant agglomeration. Although fluid dynamic viscosity changes do not affect the shape and size of particle clusters, the distance between adjacent clusters decreases at higher fluid dynamic viscosity.

Keywords Hydraulic Fracturing · Proppant and Particle Agglomeration · Fracture Intersection · Slot Experiments

Literature review
Particle agglomeration and clustering have been extensively studied for better understanding suspension behavior in chemistry and chemical engineering, but the research related to the flow and transport of proppant in realistically looking rock fractures in geo-reservoirs has been limited. Proppants are small particles used in the oil and gas industry and geothermal reservoirs during the hydraulic fracturing process. Proppants are placed into fractures by mixing and injecting with later stages of fracturing fluid to prop the fractures after the hydraulic fracturing is done. Therefore, proppants help to enhance the permeability of fractured rock mass and improve the production. Although there are several experimental studies on particle clustering in fluid-particle flows (Guala et al. 2008; Saw et al. 2008; Fiabane et al. 2012), numerical simulations prevail (Ho and Sommerfeld 2002; Raiskinmäki et al. 2003; Bec et al. 2005; Gualtieri et al. 2009; Li et al. 2011; Gustavsson et al. 2014; Reeks 2014). Proppant flow and transport in hydraulic fractures have been investigated both experimentally and numerically (Zhang et al. 2007; Dayan et al. 2009; Sahai 2012; Wong et al. 2013; Sahai et al. 2014; Aimene and Ouenes, 2015; Alotaibi and Miskimins 2015; Li et al. 2016; Luo and Tomac 2018a; Luo and Tomac 2018b; Tong and Mohanty 2016; Wen et al. 2016; Zou et al. 2016; Chang et al. 2017; Kesireddy 2017; Kou et al. 2018; Pan et al. 2018; Fjaestad and Tomac 2019; Kumar and Ghassemi 2019; Sahai and Moghanloo 2019;
Hampton et al. 2019; Nandlal and Weijermars 2019). However, only a limited number of studies have been performed on particle agglomerations during the proppant flow and transport in rock fractures (Eskin and Miller, 2008; Tomac and Gutierrez, 2014; Tomac and Gutierrez, 2015; Luo and Tomac, 2018a; Fernandez et al., 2019; Huang et al. 2019; Zhou et al., 2019).

Ho and Sommerfeld (2002) identified that particle agglomeration in turbulent flow within a collision cylinder, according to numerical models, can be described by stochastic collision model. Particle clusters are governed by collision efficiency and sticking potential due to particle geometry and size differences and van der Waals forces (Ho and Sommerfeld, 2002). Raiskinmäki (2003) studied shear flows of particulate suspension and found that clusters formed in the Couette flow can be divided into rotating chain-like clusters and particles layer at the channel wall. The size distribution of the rotating clusters is scale-invariant in the small-cluster regime and decreases rapidly above a characteristic length scale diverging at jamming transition (Raiskinmäki, 2003). In addition, the behavior of clusters can be divided into three categories based on Reynolds numbers (Raiskinmäki, 2003): When particle Reynolds number is less than 0.1, particle clusters are mostly in a chain shape and the shape is controlled by viscosity and kinetic properties; for particle Reynolds number is around 1, particle clusters occur the most frequently and the kinematic properties are losing control of cluster shapes; for particle Reynolds number is larger than 10, clusters begin to separate due to inertial effects. Bec et al. (2005) studied clustering of heavy particles in laminar flow, where each layer moves smoothly relative to neighboring layers with almost no mixings, and concluded that inertia twofold enhances collision rates: when its correlation with particle positions is high and when velocity field is not differentiable. Bec et al., 2005 proposed a model that estimates the particle collision rates with different particle sizes. Guala et al. (2008) found experimentally that large particles tend to cluster in strain-dominated regions, where the normal strain component is more significant than the rotational component when calculating velocity gradient components. Preferential particle concentrations occur at scales comparable with the Taylor microscale, which is a length scale of turbulent flow. Taylor microscale (Taylor 1935) combines the effects of the kinematic viscosity of the fluid, the root-mean square of the velocity fluctuation, and the energy dissipation rate (Guala et al. 2008). Saw et al. (2008) showed an experimental evidence of spatial particle clusters with high inertia in the homogeneous, isotropic turbulent flow at high Taylor-scale Reynolds numbers (a non-dimensional global number that describes the degree of turbulence and considers spatial and temporal scales) regime, where Taylor-scale Reynolds number is between 440 and 660. The dissipation-scale clustering becomes stronger as the fluid Stokes number increases, which is a non-dimensional number that compares relative particle inertial response time to Kolmogorov time (a time scale depends on fluid kinematic viscosity and turbulent kinetic energy dissipation rate); also, the dissipation-scale clustering shows similar trend when considering particle Stokes number (Saw et al. 2008). Guaitieri et al. (2009) did numerical simulations and concluded that the homogeneity of particle configurations in flow is broken by the interaction of local eddies. Fiabane et al. (2012) observed in experiments that neutrally buoyant particles cluster insignificantly, while heavy particles cluster a lot. Gustavsson et al. (2014) did a numerical simulation and find out that small particle clusters in incompressible random velocity fields may be strongly anisotropic and affected by gravity depending on particle Stokes number.

Generally, it has been established that proppants are not uniformly distributed in a fracture during flow and transport, and may form large vortexes across the fracture length where fluid turbulence will create multiple large spiral paths flowing in a reversed direction to flow direction due to the effect of various proppant settlement boundary shapes at the bottom (Eskin and Miller, 2008; Huang et al. 2019; Fernandez et al. 2019; Zhou et al. 2019). Investigations on effects of particle concentrations, fluid viscosity, fracture shape, and fracture roughness have been performed numerically and experimentally in the past (Tomac and Gutierrez, 2014; Tomac and Gutierrez, 2015; Luo and Tomac, 2018a). Tomac and Gutierrez (2015) found that the lubrication effect dramatically impacts particle motions when a combination of parameters is unfavorable. Lubrication forces in narrow fractures act upon particle–particle and particle–wall collisions and lead to particle agglomerations by decreasing the post-impact kinetic energy of particles. Adjacent particles stay together and form clumps, while fluid flows around clusters. As fluid viscosity and/or proppant concentration increases, agglomerations are more frequently observed. Luo and Tomac (2018a) confirmed the effects of lubrication forces experimentally and showed that proppant concentration and fluid viscosity enhance particle agglomerations in the fluid. Furthermore, wall effects at low particle diameter-to-fracture width ratios have a strong effect on agglomeration and wall effect is enhanced on rough surfaces than the smooth surfaces (Luo and Tomac, 2018a).

The main goal of this paper is to investigate the effects of fracture intersection angle, fluid flow rate, proppant volumetric concentration, and fluid dynamic viscosity on the formation of particle agglomerations using Geo—Particle Image Velocimetry–Reliability-Guided (GeoPIV-RG) Method. Proppant clustering processes during flow and transport in realistic fractures have not yet been fully understood; therefore, this paper aims to address a gap in the literature considering coupled effects of fracture intersection angle and...
other relevant parameters like the fluid dynamic viscosity, the slurry flow rate, and the initial particle concentration. By employing a relatively new video analysis approach, namely the GeoPIV-RG Method, both quantitative and qualitative information about the proppant particle motion will be obtained. Furthermore, GeoPIV-RG provides a quantitative calculation of local and relative slurry velocity field in the fracture plane, which is an important factor to assess how actual slurry motion fluctuates within the fracture under different initial and boundary (injection point velocities) conditions.

Methodology

This research uses an experimental setup to investigate different factors on proppant agglomeration, including fracture intersection angle, proppant volumetric concentration, slurry flow rate, and fluid dynamic viscosity. In this section, we will discuss how we select materials and their combinations, set up the experimental components, record, and analyze the video footages, and handle errors (Ma et al., 2020).

Material selection and experimental setup

We use sieved Ottawa F65 sand with relatively uniform size distribution at 60/100 mesh (average particle diameter is 200 μm) as the only type of proppant in all the experiments. The main factors that are varied for investigating the formation of particle clusters include the proppant volumetric concentration, the slurry flow rate, and the fluid dynamic viscosity. In this section, we will discuss how we select materials and their combinations, set up the experimental components, record, and analyze the video footages, and handle errors (Ma et al., 2020).

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Fig. 1  a Top view and b photograph of the 30° intersection angle fracture

![Fig. 1 (a) Top view and (b) photograph of the 30° intersection angle fracture](image-url)
two LED lights with 12,000 lumens are placed in front of the fracture in the left and right for enhancing light and minimizing shadow (Fig. 3b). The cameras are placed at a distance of 114 cm from the fracture front face.

The main camera used is the scientific high-resolution and high-speed PHANTOM C320. The videos were shot 1280×1024 pixels with 900 frames per second. The camera is focused to record the initial portion of the fracture immediately after the fracture intersection. A SONY DSC-RX10M3 digital still camera records fluid-particle motion prior to the intersection, whose videos are competitively high in resolution but have lower speed: 1920×1080 pixels with 60 frames per second. A Nikon D160 digital camera records all fluid-particle motions after the intersection, overlaying with the PHANTOM camera. The quality of the videos was similar to the SONY camera, 1280×720 pixels 60 frames per second. The two low-speed cameras serve as a backup.

**GeoPIV-RG method**

Geo-Particle Image Velocimetry–Reliability-Guided (GeoPIV-RG) method is typically used for analyzing motions of granular materials. GeoPIV-RG is a Matlab code developed by Stainer et al. (2015), previously called GeoPIV by White and Take (2002). Figure 4 describes the main image processing in the GeoPIV-RG. Before running

| Table 1 | Flow rates under all conditions |
|---------|--------------------------------|
| Viscosity (Pa·s) | Volumetric concentration (%) | Frequency (Hz) | Flow rate (L/min) |
| 0.001 | 10 | 10 | 3.90 |
| 0.001 | 10 | 20 | 4.55 |
| 0.001 | 20 | 10 | 3.30 |
| 0.001 | 20 | 20 | 3.70 |
| 0.005 | 10 | 10 | 3.35 |
| 0.005 | 10 | 20 | 3.68 |
| 0.005 | 20 | 10 | 2.55 |
| 0.005 | 20 | 20 | 3.50 |
| 0.010 | 10 | 10 | 2.50 |
| 0.010 | 10 | 20 | 2.50 |
| 0.010 | 20 | 10 | 2.65 |
| 0.010 | 20 | 20 | 3.13 |

| Table 2 | Parameters for all the experimental cases |
|---------|------------------------------------------|
| Test | Fluid viscosity (Pa·s) | Volumetric concentration of sand (%) | Pump rotor frequency (Hz) | Fluid flow rate (L/min) | Fracture intersection angle |
| 1 | 0.001 | 10 | 10 | 3.90 | 30 |
| 2 | 0.001 | 10 | 10 | 3.90 | 45 |
| 3 | 0.001 | 10 | 20 | 4.55 | 30 |
| 4 | 0.001 | 10 | 20 | 4.55 | 45 |
| 5 | 0.005 | 20 | 10 | 3.30 | 30 |
| 6 | 0.005 | 20 | 10 | 3.30 | 45 |
| 7 | 0.005 | 20 | 20 | 3.70 | 30 |
| 8 | 0.005 | 20 | 20 | 3.70 | 45 |
| 9 | 0.005 | 10 | 10 | 3.35 | 30 |
| 10 | 0.005 | 10 | 10 | 3.35 | 45 |
| 11 | 0.005 | 10 | 20 | 3.68 | 30 |
| 12 | 0.005 | 10 | 20 | 3.68 | 45 |
| 13 | 0.005 | 20 | 10 | 2.55 | 30 |
| 14 | 0.005 | 20 | 10 | 2.55 | 45 |
| 15 | 0.005 | 20 | 20 | 3.50 | 30 |
| 16 | 0.005 | 20 | 20 | 3.50 | 45 |
| 17 | 0.010 | 10 | 10 | 2.50 | 30 |
| 18 | 0.010 | 10 | 10 | 2.50 | 45 |
| 19 | 0.010 | 10 | 20 | 3.20 | 30 |
| 20 | 0.010 | 10 | 20 | 3.20 | 45 |
| 21 | 0.010 | 20 | 10 | 2.65 | 30 |
| 22 | 0.010 | 20 | 10 | 2.65 | 45 |
| 23 | 0.010 | 20 | 20 | 3.13 | 30 |
| 24 | 0.010 | 20 | 20 | 3.13 | 45 |
the main code, users should select the set of images to be analyzed, choose the region of interest within the selected images, and define mesh sizes and spacing. The main code tracks particle movements among images by comparing the reference and subsequent images at the point in time of interest. Both the leapfrog and sequential schemes help to provide a better result. The leapfrog method is good for experiments with no additionally marked control points and retains the initial reference image after each computation. The sequential schemes method updates the reference image after each computation, which effectively reduces wild results. Although the software directly yields the slurry velocity field, due to lack of additional markers on the fracture surface, we had to pause the software while generating displacement results in pixels. An additional post-processing converts results from displacement based to velocity based, as well as in cm/s.

**Error control**

Sources of errors in GeoPIV-RG analysis include the camera performance, the image and the video setup, the lighting condition, the setup of experimental components and the GeoPIV-RG software processing. The accuracy is also impacted by the image quality, the lighting condition, the image-particle diameter, spatial variation, recording angles, and mesh sizes (White and Take, 2002; Stanier et al. 2015;...
We developed standardized test procedures which include fixing the experiment, cameras, light, and controlling input parameters like the slurry flow rate and mixing. To avoid image distortion, the cameras are placed at the horizontal level same as the fracture and perpendicular to the fracture front face. Mesh selection is identified as the main parameter that affects the result precision. Smaller mesh sizes provide better local information while larger mesh sizes provide better precision (Stanier et al. 2015; Luo and Tomac, 2018b; Fjaestad and Tomac, 2019). To verify what mesh size and spacing are appropriate, four different mesh sizes were analyzed: 10 × 10, 20 × 20, 30 × 30, and 40 × 40 pixels. The first number is the mesh size, and the second number is the distance between the mesh centers in pixels. Two neighboring areas with similar velocity distributions are selected. The mean velocities for each selected region and mesh size are then compared. When fixing one specific region and comparing the effect of the mesh size, the error is larger than 10% between 10-pixels and 20-pixels meshes, while the error is as low as 2% between 20-pixels and 30-pixels meshes, and between 30-pixels and 40-pixels. Therefore, 20-pixels meshes and above provide sufficient precision. When fixing one specific mesh size and comparing different regions, we found that the error is larger than 10% for 10-pixels meshes, while less than 5% for 20-pixels meshes and above. For better capturing of local information, we decide to select 20-pixels meshes for our analysis. The GeoPIV-RG software analysis is run repeatedly for each experiment at least three times. All the results yielded matching graphical results within matching velocity ranges, particle cluster shapes and sizes.

The accuracy criteria is defined so that the displacement resolution is smaller than the particle size. The average of the camera pixel used is 10 μm, being 20 times smaller than the average particle diameter of 200 μm. For the 2% error considered for mesh size effects, the error in obtained slurry velocity is 0.17 cm/s, which gives a total displacement of 18 μm for 10 frames of pictures within 0.01 s. For the 5% error considered for regional effects, the velocity difference is 0.35 cm/s, which leads to a total displacement of 38 μm for 10 frames of pictures within 0.01 s. Therefore, it can be concluded that displacement errors are small comparing with the particle size.

Results

Visual and GeoPIV-RG analysis of proppant slurry flow and transport

The results of visual observation are obtained from video footage snapshots. Particle agglomeration mechanisms are barely visible in the original color pictures. Although we applied picture filtering and editing methods to enhance the contrast between particles and the surrounding background, the visual examination cannot detect observable agglomerations in most of the experiments. Figure 5a shows a snapshot of hardly observable agglomeration for experiment 23 under 30° intersection fracture, 0.01 Pa·s, 10% proppant volumetric concentration and 3.13 L/min flow rate, which is representing for most of the experiments. Figure 5b demonstrates a snapshot of clearly observable agglomeration for experiment 22 under 45° intersection fracture, 0.01 Pa·s, 20% proppant volumetric concentration and 2.65 L/min flow rate.

Therefore, the visual inspection is unhelpful for identifying particle agglomerations despite good quality images. However, GeoPIV-RG analysis of the high-resolution high-speed camera recordings provides detailed information on the microscopic scale. GeoPIV-RG captures differences at the pixel level within a series of images.

Table 3 summarizes particle agglomeration phenomena from the GeoPIV-RG and video results. Videos, as denoted in the last part in Table 3, generally have the appearance as shown in Fig. 5. Table 3 shows minor disparities in agglomeration quantity assessment between visualization and the GeoPIV-RG analysis. For example, GeoPIV-RG results yielded 3 experiments with “Plenty” of agglomerates, 13
experiments with “Medium” agglomerates, 8 experiments with “Only a few” agglomerates. Visual observation yielded 20 experiments with “Medium” quantities of agglomerates, and 4 experiments with “Only a few” agglomerates.

Selected experiments analyzed in this paper are highlighted with blue boxes. The majority of the experiments selected for further analysis, No. 18, 20, 22, 23 and 24 use high dynamic viscosity carrying fluid (No. 17–24). We use these 5 experiments to study the effect of slurry flow rate, proppant volumetric concentration, and fracture intersection angle, because high fluid dynamic viscosity experiments carry proppant clusters over the entire camera-captured region. For analyzing the effect of the carrying fluid dynamic viscosity (No. 8, 16, 24), we fix the environment under high

Table 3 Particle agglomeration summary of observations and the GeoPIV-RG results

| EXP | GeoPIV-RG results | Video results |
|-----|-------------------|---------------|
|     | exist | Obvious | Quantity | Exist | Obvious | Quantity | Other |
| 1   | Yes   | Medium | Only a few | Yes   | Medium | Medium   |
| 2   | Yes   | Clear  | Medium   | Yes   | Not Clear | Only a few |
| 3   | Yes   | Medium | Medium   | Yes   | Not Clear | Only a few |
| 4   | Yes   | Clear  | Medium   | Yes   | Medium | Only a few |
| 5   | Yes   | Clear  | Medium   | Yes   | Medium | Medium   |
| 6   | Yes   | Not Clear | Only a few | Yes   | Not Clear | Only a few |
| 7   | Yes   | Clear  | Medium   | Yes   | Medium | Medium   | Lightly Layered |
| 8   | Yes   | Clear  | Only a few | Yes   | Medium | Medium   | Lightly Layered |
| 9   | Yes   | Medium | Medium   | Yes   | Not Clear | Medium |
| 10  | Yes   | Medium | Medium   | Yes   | Not Clear | Medium |
| 11  | Yes   | Not Clear | Only a few | Yes   | Not Clear | Medium |
| 12  | Yes   | Not Clear | Only a few | Yes   | Not Clear | Medium | Lightly Layered |
| 13  | Yes   | Not Clear | Only a few | Yes   | Medium | Medium |
| 14  | Yes   | Clear  | Medium   | Yes   | Medium | Medium | Lightly Layered |
| 15  | Yes   | Clear  | Medium   | Yes   | Medium | Medium | Lightly Layered |
| 16  | Yes   | Clear  | Only a few | Yes   | Not Clear | Medium | Lightly Layered |
| 17  | Yes   | Not Clear | Only a few | Yes   | Medium | Medium | Layered |
| 18  | Yes   | Medium | Plenty    | Yes   | Not Clear | Medium | Layered |
| 19  | Yes   | Clear  | Plenty    | Yes   | Not Clear | Medium | Lightly Layered |
| 20  | Yes   | Clear  | Medium   | Yes   | Not Clear | Medium | Lightly Layered |
| 21  | Yes   | Clear  | Plenty    | Yes   | Medium | Medium | Layered |
| 22  | Yes   | Clear  | Medium   | Yes   | Medium | Medium | Layered |
| 23  | Yes   | Clear  | Medium   | Yes   | Medium | Medium | Layered |
| 24  | Yes   | Clear  | Medium   | Yes   | Medium | Medium | Layered |

Fig. 5 a Experiment without observable agglomerations; b experiment with some observable particle clusters
Effect of the proppant concentration

Effect of proppant concentration is studied on two sets of experiments: No. 18 vs 22 (Figs. 6a, b) and No. 20 vs 24 (Figs. 7a, b). This chapter analyzes the effect of proppant volumetric concentration under different slurry flow rates. Figure 6a-b shows slurry velocity analyzed with GeoPIV-RG for experiments under 45° fracture intersection angle, 0.01 Pa·s viscosity, low flow rate (2.60 L/min), and with 10% and 20% proppant volumetric concentrations. Figure 7a, b shows agglomerations of the slurry flowing under the same conditions as in Figs. 6a, b, but under a high flow rate (3.15 L/min). Figures 6a, b, 7a, b show colored plots of the slurry velocity field, with warm colors denoting higher velocities defined in the color-legend on the right side. Therefore, groups of particles which flow adjacent to each other and which exhibit similar velocity fields can be recognized and identified as flowing particle clusters. Sizes and shapes of particle clusters can be partially recognized using the GeoPIV-RG method, since the video records a two-dimensional plane at the front of the fracture. Nevertheless, GeoPIV-RG enables a better understanding of the level and the character of particle agglomerations in a relatively narrow planar fracture, where the three-dimensional effects of slurry motions across the fracture width are not dominant. Comparing Figs. 6a and 7a, qualitative differences in particle clusters size and shape are visible for lower initial 10% particle volumetric concentrations. A slower flow rate at 2.60 L/min causes larger elongated clusters toward the fracture bottom, while the faster flow rates at 3.15 L/min cause
smaller, suspended particle clusters. As the initial particle volumetric concentration increases to 20% in Figs. 6b and 7b, particle clusters become smaller, more rounded, more frequent and the flow rate difference between 2.60 L/min and 3.15 L/min hardly impacts the clustering phenomena. Frames in Figs. 6a-b and 7a-b denote different areas of interest, which are further analyzed with GeoPIV-RG method to better understand clustering phenomena at the bottom and top zones in a fracture in the case of Fig. 6a-b and middle and end sections in the case of Figs. 7a-b. For Figs. 6a-b, we categorize these subzones since there are enough horizontal trends. For Figs. 7a-b, we categorize these subzones since the horizontal trend is not clear enough, and we only select parts of the image with enough velocity contracts. Areas 1 and 2 correspond to different zones in sediment transport, dissolved load region and suspended load region, respectively, which are also present in slot flow experiments.

Figure 8a-b focuses on Area 1 as the top region of the selected experiments in Fig. 6. Suspended slurry layers are prone to forming particle clusters across concentrations and different velocity ranges. For blue regions at both 10% and 20% initial volumetric concentrations, clustering can be seen, where the size of clusters appears to be larger with a smaller number at lower initial particle volumetric concentrations. When looking at lower regions of Figs. 6a-b, as shown in Figs. 9a-b, lower volumetric concentrations also yield larger, more separated agglomerates. For the 20% initial volumetric concentration in Fig. 9b, particle agglomerates more frequently, forming smaller, more rounded and regularly shaped particle clusters, in greater number and more uniformly suspended across the observed fracture area height than for the 10% initial volumetric particle concentration in Fig. 9a.

Figure 10a, b focuses on the left regions of the selected experiments in Figs. 7a-b. Figure 11a, b focuses on the right regions of the selected experiments in Figs. 7a, b. Particle clusters in images from relatively higher flow rates of 3.15 L/min show a similar level of agglomerations across different particle volumetric concentrations. Closer observation reveals that particle cluster shapes are irregular and vary.

**Fig. 8** Top region from a Fig. 6a at 10% initial particle volumetric concentration, b Fig. 6b at 20% initial particle volumetric concentration

**Fig. 9** Bottom region from a Fig. 6a at 10% initial particle volumetric concentration, b Fig. 6b at 20% initial particle volumetric concentration

**Fig. 10** Left region from a Fig. 7a at 10% initial particle volumetric concentration, b Fig. 7b at 20% initial particle volumetric concentration
from small to large sizes, where different sizes are uniformly scattered across the fracture height at both 10% and 20% initial particle volumetric concentrations. Although proppant volumetric concentration promotes particle agglomerations under high flow rates, the effect of the increasing particle volumetric concentration is stronger under a low flow rate condition.

Effect of the slurry flow rate

Effects of the slurry flow rate during pumping into a fracture are closely studied on experiments No. 18 vs 20 (Figs. 12a-b) and No. 22 vs 24 (Figs. 13a-b). Figure 12a-b shows slurry velocity with GeoPIV-RG method for experiments under 45° fracture intersection angle, 0.01 Pa·s viscosity, low proppant volumetric concentration 10%, with fluid flow rates between 2.5 L/min and 3.2 L/min. Figure 13a-b shows agglomerations of the slurry flowing under similar conditions at 45° fracture,
0.01 Pa·s viscosity, 2.65 L/min and 3.15 L/min flow rates as in Figs. 12a-b, but under a higher proppant volumetric concentration of 20%. Warmer colors in the images have higher particle flow velocities. Therefore, we can easily identify flowing particle clusters by particle groups close to each other with similar velocities. GeoPIV-RG method captures sizes and shapes of particle groups when studying the effect of slurry flow rate. Comparing Figs. 12a and 13a, the differences in sizes and shapes of particle clusters for lower flow rates are clear (2.5 to 2.65 L/min) at different proppant volumetric concentrations. Lower proppant volumetric concentration causes particle clusters to be longer and larger, gathering around the bottom. Higher proppant volumetric concentration shapes particle clusters smaller and rounder, spreading those clusters all around the fracture. Under higher slurry flow rates (3.15 to 3.2 L/min) and different proppant volumetric concentrations, as in Figs. 12b and 13b, particle clusters are broken into even smaller and rounder shapes. Proppant volumetric concentration plays a less significant role. Frames in Figs. 12a-b and 13a-b show different areas of interest, which will be discussed later in this section. Since we have the same four experiments (No. 18, 20, 22, 24) as previous section and we are only viewing them differently, the same reason how we select the subzones is also applied in this section. Areas 1 and 2 correspond to different zones which we will further discuss in this section.

Figure 14a-b focuses on Area 1, the left region, of the experiments in Fig. 12. Under low proppant volumetric concentration, increasing flow rate significantly increases the appearance of particle clusters. A higher flow rate tends to break up larger particle clusters into smaller ones at a closer distance, which makes the general shape more complex due to this closer distance. Figure 15a-b focuses on Area 2, the right region, of the experiments in Fig. 12. The role of flow rate observed in Area 1 still holds in Area 2.

Figure 16a-b focuses on Area 1, the top region, of the experiments in Figs. 13a-b. Unlike under 10% proppant volumetric concentration, slurry flow rate does not play a strong role in forming the size and shape of particle clusters under 20% proppant volumetric concentration environment, especially for the bottom part (Area 2). Flow rate separates the distance among particle clusters a little bit under high proppant concentration conditions.

**Effect of the fracture intersection angle**

Fracture intersection angle effect on particle agglomerations is investigated in experiments No. 23 vs 24 (Figs. 18a-b). Figure 18a-b shows slurry velocity with GeoPIV-RG method for experiments under 0.01 Pa·s viscosity, 20% volumetric concentration, high flow rate at 3.13 L/min, with different intersection angles of 30° and 45°. For most of the areas, fracture intersection angle does not affect the size and shape of particle clusters. In both experiments, clusters appear small-to-medium, mostly rounded with some elongated shapes, and moderately spatially distributed in fractures. The only different part is at the very top of the fracture: for the smaller fracture intersection angle, the groups of clusters are elongated and inclined to the right. Areas 1 and 2 correspond to different zones, which we will further discuss in this section.

Figure 19a-b focuses on Area 1, the top region, of the experiments in Figs. 18a-b. Lower fracture intersection angle causes
particle clusters more inclined to the right. The shapes are rounded and elongated under both fracture intersection angles. The distances of particle clusters are moderately separated for both fractures. Figure 20a-b focuses on Area 2, the bottom region, of the experiments in Figs. 18a-b. For this region, the effect of fracture intersection angle is even less significant. We barely see any differences in sizes, shapes, and spacing of particle clusters. The effect of fracture intersection angle itself on particle agglomerations does not couple with other effects significantly.

**Effect of the fluid dynamic viscosity**

The effect of the fluid dynamic viscosity is studied on three experiments in this section, No. 08, 16, and 24 (Figs. 21a-c). Figure 21a shows the slurry velocity under 45° fracture intersection angle.
intersection angle, 20% proppant volumetric concentration, high flow rate with 20 Hz pump rotor frequency equivalent to 3.70 L/min, and 0.001 Pa·s fluid dynamic viscosity. Figure 21b shows slurry velocity under the same condition but for 0.005 Pa·s viscosity, noting that 20 Hz pump rotor frequency generates 3.50 L/min flow rate because of the elevated fluid dynamic viscosity. Figure 21c shows slurry velocity for 0.01 Pa·s fluid, noting that 20 Hz pump rotor frequency generates only 3.13 L/min flow rate. The bottom region for this set of experiments is of interest since proppant flows and settles significantly and particles are mostly absent from the top and middle parts at the lowest fluid dynamic viscosity.

Results show a clear correlation between the carrying fluid dynamic viscosity and the number of clusters, where the fluid dynamic viscosity increase leads to more clusters. Also, as fluid dynamic viscosity increases, the size of particle clusters slightly increases. However, fluid dynamic viscosity does not have a strong effect on the shape of particle clusters. The majority of particle clusters are rounded and small. Higher fluid dynamic viscosity helps to move the distance of particle clusters closer.

Conclusions

The study uses plexiglas laboratory experiments to better understand particle agglomeration and clustering mechanisms during proppant-water slurry flow through fracture intersection, including coupled effects of proppant volumetric concentration, slurry flow rates and carrying fluid dynamic viscosities on agglomeration. For experiment analysis and post-processing, high-resolution high-speed camera recorded a detailed particle flow pattern. GeoPIV-RG analysis helped to visualize particle flows and quantify velocities. By assigning a color scheme to velocity fields, potential particle clusters that have similar flow velocity within a small region were visible. Generally, it was concluded that fluid dynamic viscosity, fluid flow rate, and proppant volumetric concentration play a strong role in particle clustering processes, while the intersection angle has less effect. Also, coupled proppant volumetric concentration and fluid flow rate effects are more pronounced than other combinations of parameters.

Visual inspection is not optimal for capturing particle agglomerations with small proppant diameters. We were unable to observe potential particle clusters by visual inspection for most of the experiments; even for those experiments where we captured clusters by visual inspection, they were observable only within a certain area. GeoPIV-RG analysis of the measured velocity fields within the slurry greatly helped us to identify particle agglomerations and captures more details than visual observation. We were able to identify the size and shape, even the spacing, of particle clusters.
Carrying fluid dynamic viscosity plays a significant role in cluster formations, frequency, and shape when other factors remain unchanged. An increase in the fluid dynamic viscosity leads to more clusters and increased cluster sizes (cluster diameter from 0.25–0.5 cm at lowest viscosity to 1–1.5 cm at highest viscosity). However, the fluid dynamic viscosity does not have a strong effect on the shape of particle clusters. Although most particle clusters are rounded and small, higher carrying fluid dynamic viscosity tends to close the distance between particle clusters (cluster maximum distance from 4 cm at lowest viscosity to 1.5 cm at highest viscosity).

This study reveals for the first time that certain parameters, like the proppant volumetric concentration and the fluid flow rate, are more closely coupled with each other when governing the occurrence of particle agglomerations than other parameters. On contrary, it was also found that the fluid dynamic viscosity and the fracture intersection angle do not clearly couple with other factors regarding the formation of particle agglomeration.

When analyzing the coupled effect of the flow rate and the proppant volumetric concentration, it shall be separated into four different scenarios: lower proppant volumetric concentration with different flow rates, higher proppant volumetric concentration with different flow rates, lower flow rate with different proppant volumetric concentrations, and higher flow rate with different proppant volumetric concentrations.

When considering slurry condition under a lower proppant volumetric concentration but varying flow rates, slower flow rate causes larger (cluster diameter about 1–2 cm) and elongated clusters toward the fracture bottom, while faster flow rate causes smaller (cluster diameter about 0.25–1.5 cm) and suspended particle clusters. An increase in fluid velocity significantly decreases the size of particle clusters by breaking larger particle clusters into more approximate smaller clusters (cluster maximum distance from 2.5 cm to 0.75 cm); thus, the general shape becomes more complex.

When considering slurry conditions under a higher proppant volumetric concentration but varying flow rates, particle clusters are smaller and more rounded and occur at a larger amount of numbers, for both flow rates, comparing with lower proppant volumetric concentration condition.

When considering slurry conditions under a lower flow rate but varying proppant volumetric concentrations, less proppant volumetric concentration will have longer and larger clusters at the bottom. As proppant volumetric concentration increases, the differences in sizes and shapes of particle clusters become clearer. An increase in proppant volumetric concentration will make the agglomeration more frequent, smaller (cluster diameter from 1–2.5 cm to 0.25–1 cm), more rounded and more regularly shaped. Also, the agglomerates are more uniformly suspended across the observed fracture area.

When considering slurry conditions under a higher flow rate but varying proppant volumetric concentrations, particle clusters show a similar level of agglomeration across different proppant volumetric concentrations. An increase in proppant volumetric concentration plays a less significant role when governing the occurrence of particle agglomerations compared with lower flow rate conditions. Particle clusters are generally irregular, uniformly distributed and vary from small to large sizes. Particle clusters are broken into smaller and rounded shapes mostly due to the effect of the flow rate itself.

The effect of fracture intersection angle is the least significant factor that affects particle clustering, and the coupling effects with other factors are insignificant. We barely see any differences in sizes, shapes and spacing of particle clusters between 30° and 45° intersection angles. The shapes are both rounded and elongated in both fracture intersection angles. The distance of particle clusters is moderately separated for both fractures. For the smaller fracture intersection angle, the groups of clusters are inclined to the right in the top region.

Maintaining a good proppant transport behavior is very critical in hydraulic fractures. Proppant agglomeration is one of the threats to a good transport performance. Since viscosity helps to transport proppant at further distance while it also causes more agglomeration which may causing clogging, we suggest caution when using carrying fluid with very high viscosity. Since fracture intersection angle does not have a strong effect on particle agglomeration, we do not worry about how fracture geometry will cause potential clogging due to particle agglomeration. Since proppant volumetric concentration and fluid flow rate are coupled with each other, we suggest using lower proppant concentration at a higher fluid flow rate to minimize the occurrence of proppant agglomeration and limit the size of agglomeration.

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**Data availability** All authors make sure that all data and materials as well as software application or custom code support their published claims and comply with field standards.

**Code availability** Upon request.
Declarations

Conflict of interest  The authors have no conflicts of interest to declare that are relevant to the content of this article.

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