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Impact of the surface phase transition on magnon and phonon excitations in BiFeO₃ nanoparticles

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We have performed Raman scattering measurements on BiFeO₃ nanoparticles and studied both magnetic and lattice modes. We reveal strong anomalies between 140 K and 200 K in the frequency of magnon and E(LO₁), E(TO₁) and A₁(LO₁) phonon modes. These anomalies are related to a surface expansion and are enhanced for nanoparticle sizes approaching the spin cycloidal length. These observations point out the strong interplay between the surface, the lattice, and the magnetism for sizes of BiFeO₃ nanoparticles close to the cycloid periodicity.

Bismuth ferrite (BiFeO₃) represents a prototypical multiferroic with outstanding properties. This multifunctional material has been associated with a number of diverse technological applications such as photovoltaics,¹,² electrocatalysis,³ nanoelectronics,⁴,⁵, energy harvesting,⁶ and even spintronics.⁷,⁸ Also, it has been demonstrated that controlling the dimensionality of this material allows us to modify its properties. For example, controlling the size of BiFeO₃ nanoparticles permits a significant tuning of the magnetic, electrical, and optical properties.⁸,¹⁰ Moreover, it has been proposed that the confinement in BiFeO₃ nanoparticles should induce a size-dependent bistability of magnetization and polarization useful for memory bits.¹¹

In bulk phase, BiFeO₃ is ferroelectric below the Curie temperature \( T_C \approx 1100 \text{ K} \) with a large spontaneous electrical polarization of \( \sim 100 \mu \text{C-cm}^{-2} \) (see Fig. 1(a)).¹²,¹³ The electrons present at the Bi sites are responsible for the cationic displacements at the origin of the ferroelectricity.¹⁴,¹⁵ In addition, an antiferromagnetic order appears below the Néel temperature, \( T_N \approx 640 \text{ K} \). This magnetic order corresponds to a G-type antiferromagnetic behavior, modulated by a long-wavelength cycloid of 62 nm.¹⁶ This modulation is attributed to a homogeneous Dzialoshinskii-Moriya interaction activated by the ferroelectric displacement of the Fe sites.¹⁷,¹⁸ The cycloid is also slightly tilted out of its propagation plane and characterised by a local ferromagnetic moment cancelled out over a period.¹⁹ This additional modulation is due to an inhomogeneous Dzialoshinskii-Moriya interaction activated by the rotation of oxygen octahedra.¹⁸,¹⁹ Reducing the size of ferroelectric nanoparticles induces structural distortions which favor the high-symmetry paraelectric phase. In the case of BiFeO₃, it has been determined that the paraelectric phase appears below 9-10 nm.²¹,²² For antiferromagnetic nanoparticles, the uncompensated antiferromagnetic sublattice at the surface leads to a ferromagnetic moment which increases as the size is reduced.²³,²⁴ Unexpectedly, F. Huang et al. have observed an anomalous behavior of the magnetization for a size close to the cycloid periodicity.²⁵ In addition, a surface expansion takes place between 140 K and 200 K within the topmost 10 nm of the bulk.²⁶

The role of the surface expansion on the dynamical properties of BiFeO₃ nanoparticles, for which the surface/volume ratio increases as the size is reduced, remains to be studied. In this work, we have tracked the effect of the surface expansion by the corresponding size reduction on phonons and magnons. We observe the disappearance of the fingerprint of the cycloidal spin excitations between the sizes of 83 nm and 61 nm. At two different temperatures associated with surface expansion, anomalies in the frequency of magnetic and lattice excitations are observed. Such anomalies are enhanced for a nanoparticle size close to the cycloid periodicity.

We performed Raman spectroscopy measurements on BiFeO₃ nanoparticles. Five sizes have been synthesized by the sol-gel method which has been adapted and optimized from the protocol reported in Ref. 19: 250 nm \( \pm 100 \text{ nm} \), 158 nm \( \pm 17 \text{ nm} \), 83 nm \( \pm 20 \text{ nm} \), 61 nm \( \pm 9 \text{ nm} \), and 31 nm \( \pm 7 \text{ nm} \). Figure 1(b) shows a transmission electron microscopy (TEM) image of nanoparticles with a mean size of 83 nm. The nanoparticles are regularly shaped and approximately spherical. Figure 1(c) presents a magnification of the region defined in Fig. 1(b). The Fourier transform shows the presence of sharp diffraction spots which are indicative of the formation of single crystalline BiFeO₃. Platelets of nanoparticles

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with a thickness of 3 nm have been prepared under very low pressure for Raman measurements. Raman spectra were recorded in a backscattering geometry with a triple spectrometer Jobin Yvon T64000 using the 647.1 nm excitation line from an Ar+–Kr+ mixed gas laser. The penetration depth of the laser light is very large because of the low extinction coefficient $k = 1.2 \times 10^{-4}$ of BFO. Thus, BFO is nearly transparent for the 647.1 nm light. The excited volume is given by the focus ($\sim 70 \mu m$). The high rejection rate of the spectrometer allows us to detect excitations as low as 10 cm$^{-1}$. Temperature is controlled with an open cycle He cryostat. Since nanoparticles are randomly oriented, there are no Raman selection rules. We observe all the phonon modes that characterize the rhombohedral phase (R3c) for each nanoparticle size.

Figure 2(a) shows the low-energy part of the Raman spectra for the five sizes of nanoparticles. For 250 nm, three peaks are observed. In the bulk phase, the magnetic cycloid manifests itself by two series of narrow peaks in the Raman spectra. They are the fingerprint of the magnon modes. They correspond to the spin excitation oscillations in and out of the cycloidal plane measured at zero wave vector. The peaks observed in Fig. 2(a) correspond to the superposition of the narrow peaks of the bulk (no Raman selection rules in randomly oriented nanoparticles) and are associated with the cycloidal spin states. For 158 nm and 83 nm, we distinctly only observe two peaks. No peak is detected for sizes of 61 nm and 31 nm. The optical gap of BiFeO$_3$ shifts with the nanoparticle size which could explain the disappearance of the peaks. However, the signature of the cycloid has not been detected using any other laser wavelengths. In Fig. 2(b), we have reported the frequency of the magnon at 17 cm$^{-1}$ as a function of temperature. For 250 nm, the frequency has a similar dependence as a magnetic excitation in the bulk phase. For 158 nm, the frequency presents a jump around 140 K and a plateau around 200 K. A slightly more pronounced trend is measured for a size of 83 nm. In the same range of temperature, a surface phase transition with an associated sharp change in lattice parameter at the surface has been observed. This “skin” effect is estimated to be within the topmost 10 nm of BFO. For a nanoparticle size of 80 nm, this effect represents 33% of the volume of the nanoparticle. The observed anomalies in the magnon frequencies of nanoparticles can be attributed to the surface expansion. The effect of this expansion on the spin excitations is enhanced around 83 nm. Hence, our results show that the surface has a significant impact on the magnetism for a size approaching the cycloid periodicity of 62 nm. It is known that BiFeO$_3$ shows a strong magnetostriction and
spin-phonon coupling. Both phenomena might be at the origin of the observed anomalies. This raises the question of the impact of the surface expansion in nanoparticles on the lattice excitations when the size approaches the cycloid periodicity.

Figure 3(a) shows the Raman spectra of the $E(TO_1)$ and $E(LO_1)$ phonons at 75 cm$^{-1}$ and 81 cm$^{-1}$ respectively for the five sizes. The temperature dependence of the $E(TO_1)$ phonon is responsible for the variation of the dielectric constant and is a potential candidate to be the soft mode driving the ferroelectric transition. It has been observed in infrared spectroscopy that, compared to that of the $E(LO_1)$ phonon, the intensity of the $E(TO_1)$ phonon decreases for sizes smaller than 83 nm. This behavior has been ascribed to the depolarization of the nanoparticles. This size-dependent intensity can be expressed as a function of the inverse nanoparticle diameter. The critical size below which the nanoparticles become paraelectric can be determined using this relation and the relative intensity of the $E(TO_1)$ and $E(LO_1)$. We find a critical size of 12 nm in agreement with previous measurements around 10 nm.

Figure 3(b) shows the Raman spectra of the $A_{1}(LO_1)$ and $A_{1}(LO_2)$ phonons at 148 cm$^{-1}$ and 177 cm$^{-1}$ respectively for the five sizes. The temperature dependencies of their frequency are plotted in Fig. 5. The frequencies of the $A_{1}(LO_2)$ mode present the same size dependent anomalies (jump and plateau) as the ones measured for the $E(LO_1)$ mode. Notice that the other phonons, such as the $A_{1}(LO_2)$ mode, exhibit a classical behavior for each size corresponding to the thermal expansion of the lattice.

The frequencies of the two phonons are reported in Fig. 4. To have access to the frequency of the $E(TO_1)$ mode, the $E(LO_1)$ is subtracted by a Fano shape. Notice that the $E(TO_1)$ mode is too low in intensity to be studied as a function of the temperature for the sizes below 83 nm. In Fig. 4(a) and (c), the temperature dependence of the frequencies for the 250 nm is similar to the one observed in the bulk. For 158 nm, both mode frequencies present a jump at around 140 K followed by a plateau at around 220K (Fig. 4(b) and (d)). This behavior is even more pronounced for 83 nm. At 61 nm, the presence of the jump and the plateau are less obvious in the frequencies of $E(LO_1)$. They disappear for a size of 31 nm for which the temperature dependence of the frequency is close to the one at 250 nm. The surface phase transition no longer plays a role for a size of 31 nm.

These measurements show that there is an unusual trend associated with particular sizes. First of all, we note the disappearance of the fingerprint of the cycloidal spin excitations between the sizes of 83 nm and 61 nm. Moreover, the frequency of the magnetic excitations and the frequency of the $E(LO_1)$, $E(TO_1)$ and $A_{1}(LO_1)$ phonons present identical anomalies at the same temper-
atures related to the surface expansion. In addition, the anomalies are enhanced for 83 nm and disappeared for 31 nm. We remark that the only comparable physical scale to these peculiar sizes is the periodicity of the cycloid (62 nm).

The first question that arises is the critical size of the nanoparticles below which the spiral of spins is either strongly modified or suppressed. From an experimental point of view, previous Mössbauer spectroscopy measurements have detected the cycloid state for a size of 54 nm. The modification of the cycloid can come from the uncompensated spins at the surface and the magnetic surface anisotropies. However magnetic surface anisotropies can dominate magnetic properties only in very small nanoparticles and the cycloid should adapt itself. The disappearance of the Raman signature of the cycloid can come from the uncompensated spins at the surface and the magnetic surface anisotropies. However magnetic surface anisotropies can dominate magnetic properties only in very small nanoparticles and the cycloid should adapt itself. The disappearance of the Raman signature of the cycloid can come from the uncompensated spins at the surface and the magnetic surface anisotropies. 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