Numerical Well Testing Interpretation Model and Applications in Crossflow Double-Layer Reservoirs by Polymer Flooding

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1. Introduction

Over the past several decades, many EOR methods were researched in laboratories and oilfields to improve oil recovery, for example, polymer flooding [1], surfactant flooding [2], alkali-surfactant-polymer (ASP) flooding [3], nanoparticles [4, 5], low salinity water flooding [6], and CO₂ [7, 8]. However, polymer flooding is most commonly applied in oilfields, especially hydrolyzed polyacrylamide (HPAM) polymer flooding because of its low cost and high efficiency [9]. The oil recovery of polymer flooding is enhanced mainly by increasing sweep efficiency [10].

Conventional pressure transient test has historically been the main application of permeability and skin estimation in oilfields, by using a pressure gauge positioned at a fixed depth in a well. The pressure test of multilayered reservoir was studied from the 1960s; however, the research on the individual production of multilayered reservoir was not carried out due to the restriction of testing tools and technology. A percolation model of multilayered reservoir was derived in 1961, and the wellbore pressure and production of individual layers were also deduced [11]. This model considered that the interlayer had different parameters but neglected the wellbore storage effect. In 1978, a new model was further developed to get the wellbore pressure solution in real space for multilayered reservoir by using Stehfest algorithm [12]. It took the wellbore storage and skin factor into account, whereas it ignored the crossflow of wellbore pressure response. From the 1980s to 1990s, many researchers interpreted well testing data by analysis of measured wellbore pressure and stratified
flow rate. With the help of multilayer testing techniques, the expression of pressure solution was established through the relationship between wellbore pressure and stratified flow rate of multilayered reservoirs [13, 14]. The well testing model of crossflow double-layer reservoir was put forward in 1985 [15], which was further investigated by theoretical study of flow mechanics [16]. However, the type curves of crossflow double-layer reservoirs were not established. The problem of interlayered crossflow in a stratified reservoir was mathematically simplified by employing a semipermeable wall model [17]. Based on the former research, the dynamic model and exact solution of bottom hole pressure were proposed. Most researches on well testing and fluid percolation in double-layer reservoirs were based on analysis method to get the analytic solution of bottom hole pressure (BHP). In recent years, the numerical methods were employed to study well testing problems of multilayered reservoir with the help of rapid development of computer technology [18–21].

HPAM polymer solution is one kind of non-Newtonian fluids, and its viscosity is a significant parameter used to establish well testing interpretation model for polymer flooding. Many researches on the rheological behavior of polymer solution simply consider polymer as power law fluid and using constant power exponent model to represent the percolation of polymer solution in reservoirs [22–25], which is unable to meet the actual demands of our oilfields. For crossflow double-layer reservoirs by polymer flooding, there exist not only shear effect and viscoelastic effect but also physic-chemical interaction during polymer solution percolating in porous medium, whereas the constant power exponent viscosity model ignores diffusion and convection of polymer during transport in porous medium. Meanwhile, the adsorption of polymers in the porous medium results in the average of viscosity and its viscosity at infinite shear rate is pretty close to brine viscosity; γ1/2 is the shear rate at which apparent viscosity is the average of μ∞ and μp; γ is the effective shear rate; P are fitting parameter (usually 1.0 < Pa < 1.8); μp is the viscosity at very low shear rate, which is calculated by modified Flory-Huggins equation [35]:

\[ \mu_p = \mu_w \left[ 1 + (A_1 C_p + A_2 C_p^2 + A_3 C_p^3) C_{SEP}^{SP} \right], \]  

where μp is apparent viscosity of polymer solution; μ∞ is viscosity of polymer solution at infinite shear rate, which is simplified as brine viscosity (μw) and satisfied the accuracy in this study since polymer concentration is relatively low and its viscosity at infinite shear rate is pretty close to brine viscosity; γ1/2 is the shear rate at which apparent viscosity is the average of μ∞ and μp; γ is the effective shear rate; P are fitting parameter (usually 1.0 < Pa < 1.8); μp is the viscosity at very low shear rate, which is calculated by modified Flory-Huggins equation [35]:

\[ \mu_p = \mu_w \left[ 1 + (A_1 C_p + A_2 C_p^2 + A_3 C_p^3) C_{SEP}^{SP} \right], \]  

where A1, A2, and A3 are fitting parameters obtained from matching experimental data; C_p is polymer concentration; C_{SEP}^{SP} Represents the effect of salinity and hardness on polymer viscosity.

Since temperature significantly affects rheological behavior of polymer and the effect of pressure on polymer viscosity is negligible compared with temperature, the polymer solutions were prepared by mechanical stirring at 75 °C to simulate reservoir temperature. The tested polymer concentrations range from 100 mg/L (0.1 g/L or 0.01 wt%) to 4000 mg/L (the polymer concentrations in our field tests are between 1600 mg/L and 2500 mg/L). The polymer rheological measurement was carried out by Haake RS6000 rheometer made in Germany. The viscosity of polymer solutions with different concentrations was measured at 75 °C to get the fitting numbers of A1, A2, and A3, shown in Figure 1 and Table 2. The measurements were performed under 0.01 s⁻¹ shear rate, since μp₀ is the viscosity at very low shear rate.

\[ P_a = 1.182 \left( \mu_p^0 \right)^{0.0341}, \]  

\[ \gamma_{1/2} = 376.2 \left( \mu_p^0 \right)^{-1.365} + 0.0341i. \]
The relationship between effective shear rate $\gamma$ and seepage velocity is shown in the following [36]:

$$\gamma = \frac{3n + 1}{n + 1} \frac{10^4 \nu}{\sqrt{8C^2 K \phi}},$$  

and

$$\nu = \frac{Q}{2\pi rh},$$

where $n$ is the bulk power law index, in the range of 0 to 1; $C'$ is tortuosity coefficient; $\phi$ is porosity; $K$ is permeability; $Q$ is flow rate of injected polymer solution; $h$ is reservoir thickness; $r$ is radial distance; $\nu$ is Darcy velocity.

By considering IPV and permeability reduction caused by polymer flooding, (5) is changed to

$$\gamma = \frac{3n + 1}{n + 1} \frac{10^4 \nu}{\sqrt{8C^2 K_p \phi_p}},$$

where $K_p$ is effective permeability, $K_p = K/R_k$, $R_k$ being permeability reduction coefficient; $\phi_p$ is effective porosity, $\phi_p = \phi(1 - IPV)$.

During transport in porous medium, polymer concentration is also affected by convection and diffusion. Thus, polymer concentration by considering convection and diffusion is shown in the following [37]:

$$C_p (r, t) = \frac{C_{p0}}{2} - \frac{C_{p0}}{2} \text{erf} \left[ \frac{r - Vt}{2\sqrt{Df}} \right],$$

where $C_{p0}$ is initial polymer concentration; $D$ is diffusion coefficient.

There are several shear-thinning rheological models developed for polymer solutions. The model used in this study can accurately match the apparent viscosity of the proprietary HPAM polymer provided by CNPC over a wide range of injected velocity, especially when polymer solutions pass through the perforation.

### 3. Well Testing Modeling Methodology

The percolation of polymer flooding in crossflow double-layer reservoir is sketched in Figure 2. Crossflow occurs in the interlayer and fluids can transport from low permeability zone to high permeability zone when polymer solutions are injected into the reservoir. The hypotheses are as follows: (1) polymer solutions and reservoir brines are miscible; (2) properties of polymer solutions are the same in each layer; (3) fluids flow satisfies Darcy’s law; (4) each layer is homogeneous, but formation properties, for example, layer thickness, permeability, skin factor, and compressibility, are different between two layers; (5) gravity effect is negligible; (6) the initial pressure of each layer is the same, $p_i$; (7) reservoir rocks and fluids are compressible; (8) process of polymer transportation is isothermal; (9) crossflow of interlayer is pseudosteady state.

Based on the rheological model and hypotheses discussed above, the well testing interpretation model in crossflow double-layer reservoir by polymer flooding is established, by considering shear, diffusion, convection, IPV, permeability reduction, wellbore storage effect, and different layered skin factors:

(i) percolation equation:

$$K_p h_1 \frac{\partial}{\partial r} \left( r \frac{1}{\mu_p} \frac{\partial p_1}{\partial r} \right) + a \frac{K_p h_2}{\mu_p} (p_2 - p_1) = \phi_p C_{p1} h_1 \frac{\partial p_1}{\partial t},$$

$$K_p h_2 \frac{\partial}{\partial r} \left( r \frac{1}{\mu_p} \frac{\partial p_2}{\partial r} \right) - a \frac{K_p h_2}{\mu_p} (p_2 - p_1) = \phi_p C_{p2} h_2 \frac{\partial p_2}{\partial t};$$

(ii) internal boundary conditions:

wellbore storage effect

$$qB = C \frac{dp_w}{dt} - \left( \frac{K_p h_1}{\mu_p} r \frac{\partial p_1}{\partial r} + \frac{K_p h_2}{\mu_p} r \frac{\partial p_2}{\partial r} \right) \bigg|_{r=r_w},$$

skin factor

$$p_w(t) = \left( p_1 - s_1 r \frac{\partial p_1}{\partial r} \right) \bigg|_{r=r_w} = \left( p_2 - s_2 r \frac{\partial p_2}{\partial r} \right) \bigg|_{r=r_w};$$

(iii) external boundary condition (infinite boundary):

$$p_1 (\infty, t) = p_2 (\infty, t) = p_i;$$

### Table 2: Characteristics of polymer solutions.

| $\mu_w$ (mPa·s) | $A_1, (g/L)^{-1}$ | $A_2, (g/L)^{-2}$ | $A_3, (g/L)^{-3}$ | $C_{p0}, (g/L)$ | $D, (cm^2/s)$ |
|-----------------|------------------|------------------|------------------|----------------|---------------|
| 0.5             | 0.642            | 0.201            | 0.931            | 1.750          | 0.0246        |

![Figure 1: Relationship between polymer viscosity ($\mu_p$) and polymer concentration ($C_p$) at 75°C under 0.01 s⁻¹ shear rate.](image)
4. Type Curves and Sensitivity Analysis

Based on dimensionless BHP and dimensionless BHP derivative, the type curves of pressure and pressure derivative in log-log scale are obtained. Sensitivity analysis is further investigated.

4.1. Type Curves. Type curves of well testing in crossflow double-layer reservoir by polymer flooding are shown in Figure 3, which shows that type curves have five flow segments: (I) wellbore storage section, where pressure and pressure derivative curves are superposed, reflecting the pressure response characteristics during well storage stage; (II) intermediate flow section (transient section), that describes the pressure response from pure wellbore storage stage to mid-radial flow stage within internal region, and there is a “convexity”; (III) mid-radial flow section, where fluids flow of individual layer achieves plane radial flow before crossflow happens, showing a horizontal period of pressure derivative line; (IV) crossflow section, where fluids in low permeability layer transport through interlayer into high permeability layer, and there is a “concave”; and (V) systematic radial flow section, where the whole system presents plane radial flow over time and the pressure curve lightly turns upward due to the influence of the non-Newtonian fluid properties of polymer solution.

The comparison of type curves in double-layer reservoir by polymer flooding with and without crossflow is demonstrated in Figure 4. It is obvious that there exists a “concave” (section IV) in the crossflow double-layer reservoir, which is formed by the fluids percolation from low permeability layer into high permeability layer resulting in crossflow through the interlayer. After crossflow is developed over time, the “concave” will vanish and curves will overlap when pressures of each layer achieve equilibrium. In systematic radial flow section (V), the BHP in crossflow reservoir is lower than that in noncrossflow reservoir since crossflow reduces the flow resistance (equal to systematic permeability enhanced); however, the BHP derivative is the same with value of 0.5.

4.2. Sensitivity Analysis. The effects of different parameters on type curves are investigated, including interporosity flow coefficient, ratio of formation coefficient, storativity ratio, initial polymer concentration, and IPV.

4.2.1. Interporosity Flow Coefficient. The influence of interporosity flow coefficient (λ) on type curves in crossflow double-layer reservoir by polymer flooding is shown in Figure 5. Smaller λ indicates fewer fluids transport through interlayer, which depends on the permeability difference and BHP difference between two layers. Smaller permeability difference or BHP difference results in small a and λ. The “concave” appears delayed with smaller interporosity flow coefficient since it needs more time for the fluids in crossflow section (IV) to achieve equilibrium. After that, individual layer reaches the plane radial flow and BHP derivative curve changes to horizontal, indicating fluids flow achieves systematic radial flow section (V). The time of “concave” appearance
can qualitatively evaluate formation heterogeneity since it is influenced by layered permeability difference: it appears earlier in heterogeneous formation, and it appears later in relative homogenous formation.

**4.2.2. Formation Coefficient Ratio.** Figure 6 represents the effect of formation coefficient ratio ($\chi$) on type curves in crossflow double-layer reservoir by polymer flooding. It shows that $\chi$ only affects the crossflow section (IV): the smaller $\chi$ is, the shallower the “concave” becomes and vice versa. For reservoirs with fixed value of layer permeability, smaller $\chi$ means smaller difference of layer thickness, and the “concave” becomes shallower as permeability difference decreases.

**4.2.3. Storativity Ratio.** The effect of storativity ratio ($\omega$) on type curves in crossflow double-layer reservoir by polymer flooding is shown in Figure 7. The width and depth of the “concave” are influenced by $\omega$: the “concave” gradually becomes narrower and shallower when $\omega$ increases, and vice versa. Individual layers, respectively, reach their radial flow
4.2.4. Initial Polymer Concentration. The effect of initial polymer concentration ($C_{p0}$) on type curves in crossflow double-layer reservoir by polymer flooding is shown in Figure 8, which indicate that the crossflow section (IV) appears later and BHP derivative curve in systematic radial flow section (V) turns more upward by increasing $C_{p0}$. Since viscosity is increased for higher $C_{p0}$, there is more flow resistance for fluids to transport through interlayer, resulting in delay of crossflow section (IV) appearance and greater amplitude of BHP derivative curve in systematic radial flow section (V). Consider $C_0 = 0$ mg/L expressed as water flooding, which is Newtonian fluid with constant viscosity. Further investigation indicates that the effect of polymer rheology on type curve section (V) is dramatically reduced by crossflow, which means the pressure curve and pressure derivative curve of polymer flooding are similar to those of water flooding in section (V) and this phenomenon is also proved by field test data. However, the slope of type curves in one-layer reservoir with homogenous thickness by polymer flooding is much larger than that of water flooding.

4.2.5. Inaccessible Pore Volume. Figure 9 represents the effect of IPV on type curves in crossflow double-layer reservoir by polymer flooding. The crossflow section (IV) appears earlier for reservoir with bigger IPV. Bigger IPV means lower effective porosity, and the fluid velocity is higher for the reservoir with fixed flow rate of polymer injected, resulting in earlier appearance of the crossflow section (IV) and systematic radial flow section (V). However, the effect of IPV on well testing type curves is unremarkable; moreover, the IPV caused by polymer flooding in oilfields is usually less than 0.15, so the effect of IPV can be negligible during well testing interpretation. Unlike other parameters, the effect of IPV on type curves is listed here only for theoretical analysis.

4.2.6. Wellbore Storage Coefficient. The effect of wellbore storage coefficient on type curves in crossflow double-layer reservoir by polymer flooding is shown in Figure 10. The depth of the “concave” and “convexity” is influenced by $C_0$; however it does not affect the width. The crossflow section (IV) and systematic radial flow section (V) gradually appear earlier with $\omega$ increases; meanwhile, the mid-radial flow section (III) is shortened.
5. Field Tests Interpretation

Well testing data of field test was provided by CNPC. Then draw the BHP data with time in log-log scale. Interpret the data and perform history matching of type curves to evaluate reservoir formation and calculate the average formation pressure, layered permeability, layered skin factor, and wellbore storage coefficient. The interpretation results of layered permeability and layered skin factor are significant for oilfields, since oil industry will adjust development plan of production based on them. If the layered permeability is much lower or the layered skin factor is much higher than those of before polymer flooding, it indicates that polymer flooding leads to serious formation damage and specific methods should be employed to reduce formation damage and improve production, for example, acidizing.

5.1. Basic Properties of Oilfield. The tectonic surface area is 33 km², and structure amplitude is about 100 m. The formation conditions and fluid properties are suitable for polymer flooding; meanwhile, relatively low salinity and low divalent cation concentration are beneficial to maintaining systematic viscoelasticity. The characteristics of crude oil under surface conditions and reservoir conditions are shown in Tables 3 and 4, respectively. The pressure derivative curve of field test data was modified for curve smoothing by using Bourdet’s method [38].

5.2. Field Test One. Well testing was based on injection fall-off process. The polymer solutions were injected into double-layer reservoirs with initial concentration of 1600 mg/L, and the reservoir thickness is 14 m. Well 5-227 performed polymer flooding from Feb 1, 2012, to May 7, 2012, and then the polymer injection was stopped and pressures were measured. It took three days for well testing, and polymer flooding was performed again since May 10, 2012. Basic parameters of well and reservoir are shown in Table 5.

The history matching curves and field testing data are shown in Figure 11, and the interpretation results are shown in Table 6. The permeability and skin factor of individual layer acquired by interpreting field test data are consistent with the actual situation of oilfield, indicating that our model can accurately interpret Field Test One and evaluate formation. Meanwhile, polymer flooding results in negligible permeability reduction or formation damage in this case, since the interpreted permeability and skin factors are nearly the same as those of before polymer flooding.

5.3. Field Test Two. Well testing was also based on injection fall-off process. The polymer solutions were injected into double-layer reservoirs with initial concentration of 1600 mg/L, and the reservoir thickness is 21 m. Well 5-225 (500 meters away from Well 5-227) performed polymer flooding from Feb 1, 2012, to Apr. 28, 2012, and then the polymer injection was stopped and pressures were measured (nine days before Field Test One). It took three days for well testing, and polymer flooding was performed again since May 1, 2012. Basic parameters of well and reservoir are shown in Table 7.

The history matching curves and field testing data are shown in Figure 12, and the interpretation results are shown in Table 8. The occurrence of “concave” is earlier than Field Test One, due to the bigger permeability difference between two layers. The skin factor of individual layer and layer 1 permeability acquired by interpreting field test data are consistent with the actual situation of oilfield, which further prove that our model can accurately interpret Field Test Two and evaluate formation. Moreover, the layer 2 permeability is 68 mD and permeability reduction coefficient is 3.1 on average, indicating formation was damaged by polymer flooding. Blockage removal agent was further injected into the reservoir and layer 2 permeability was increased to 174 mD, resulting in 2.4% EOR of individual well.

6. Conclusion

This work established well testing models for crossflow double-layer reservoirs by polymer flooding. Type curves of numerical well testing were obtained, and field test data
Figure 11: Field test data and history matching of type curves (Field Test One: Well 5-227).

Table 5: Basic parameters of well and reservoir for 5-227 field test.

| Parameter                        | Value |
|----------------------------------|-------|
| Injection rate                   | 100   |
| Layer 1 thickness                | 8     |
| Layer 2 thickness                | 6     |
| Oil volume factor                | 1.1037|
| Porosity                         | 0.3   |
| Crude oil viscosity              | 14.2  |
| Brine viscosity                  | 0.5   |
| Temperature                      | 75    |
| Total compressibility            | 0.0014|
| Well radius                      | 0.1   |
| Layer 1 permeability before polymer flooding | 1592  |
| Layer 2 permeability before polymer flooding | 1466  |
| Layer 1 skin factor before polymer flooding | n/a   |
| Layer 2 skin factor before polymer flooding | n/a   |

Table 6: Interpretation results of Field Test One (Well 5-227).

| Parameter                        | Value |
|----------------------------------|-------|
| Average reservoir pressure       | 18.56 |
| Layer 1 permeability             | 1340  |
| Layer 2 permeability             | 68    |
| Layer 1 skin factor              | 2.56  |
| Layer 2 skin factor              | 1.98  |
| Wellbore storage coefficient     | 0.54  |

Table 7: Basic parameters of well and reservoir for 5-225 field test.

| Parameter                        | Value |
|----------------------------------|-------|
| Injection rate                   | 136   |
| Layer 1 thickness                | 12    |
| Layer 2 thickness                | 9     |
| Oil volume factor                | 1.1037|
| Porosity                         | 0.25  |
| Crude oil viscosity              | 14.2  |
| Brine viscosity                  | 0.5   |
| Temperature                      | 75    |
| Total compressibility            | 0.0014|
| Well radius                      | 0.1   |
| Layer 1 permeability before polymer flooding | 1352  |
| Layer 2 permeability before polymer flooding | 211   |
| Layer 1 skin factor before polymer flooding | n/a   |
| Layer 2 skin factor before polymer flooding | n/a   |

Table 8: Interpretation results of Field Test Two (Well 5-225).

| Parameter                        | Value |
|----------------------------------|-------|
| Average reservoir pressure       | 17.26 |
| Layer 1 permeability             | 1570  |
| Layer 2 permeability             | 1460  |
| Layer 1 skin factor              | 1.13  |
| Layer 2 skin factor              | 1.20  |
| Wellbore storage coefficient     | 0.60  |

were further interpreted and history-matched. The main conclusions drawn from this study are as follows.

1. The model developed in this work by considering IPV, permeability reduction, shear rate, diffusion, and convection can accurately demonstrate rheological behavior of the proprietary HPAM polymer provided by CNPC over a wide range of injected velocity, especially when polymer solutions pass through the perforation.

2. Type curves have five sections with different flow status: (I) wellbore storage section, where pressure and pressure derivative curves are superposed, reflecting the pressure response characteristics during well storage stage; (II) intermediate flow section (transient section between wellbore storage section and mid-radial flow section); (III) mid-radial flow section, where fluids flow of each layer achieves plane radial flow before crossflow occurs; (IV) crossflow section where fluids in low permeability layer transport through interlayer into high permeability layer; and (V) systematic radial flow section, where the whole system presents plane radial flow over time.

3. The remarkable feature of the crossflow in type curves is the occurrence of “concave.” The effect of polymer rheology on type curve section (V) is dramatically reduced by crossflow, which means the pressure curve and pressure derivative curve of polymer flooding are similar to those of water flooding in systematic radial flow section (V). Sensitivity analysis was performed to investigate the effect of different parameters on the type curves, including interporosity flow coefficient,
formation coefficient ratio, storativity ratio, initial polymer concentration, IPV, and wellbore storage coefficient. The influence of IPV on the well testing in polymer flooding reservoirs can be neglected, since polymer flooding usually results in unremarkable IPV.

(4) Field tests were conducted in two wells of crossflow double-layer reservoirs by polymer flooding. The field test data were interpreted and history-matched by employing our well testing interpretation method, which indicated our model can accurately interpret field test data and evaluate formation. Moreover, formation damage caused by polymer flooding can also be evaluated by comparison of the interpreted permeability with initial layered permeability before polymer flooding. If interpreted permeability is much lower than initial permeability, specific techniques should be employed to eliminate formation damage and enhance oil recovery.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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