Deep-ocean mixing driven by small-scale internal tides

Clément Vic1,8, Alberto C. Naveira Garabato1, J.A. Mattias Green2, Amy F. Waterhouse3, Zhongxiang Zhao4, Angélique Melet5, Casimir de Lavergne6, Maarten C. Buijsman7 & Gordon R. Stephenson7

Turbulent mixing in the ocean is key to regulate the transport of heat, freshwater and biogeochemical tracers, with strong implications for Earth’s climate. In the deep ocean, tides supply much of the mechanical energy required to sustain mixing via the generation of internal waves, known as internal tides, whose fate—the relative importance of their local versus remote breaking into turbulence—remains uncertain. Here, we combine a semi-analytical model of internal tide generation with satellite and in situ measurements to show that from an energetic viewpoint, small-scale internal tides, hitherto overlooked, account for the bulk (>50%) of global internal tide generation, breaking and mixing. Furthermore, we unveil the pronounced geographical variations of their energy proportion, ignored by current parameterisations of mixing in climate-scale models. Based on these results, we propose a physically consistent, observationally supported approach to accurately represent the dissipation of small-scale internal tides and their induced mixing in climate-scale models.
he deep ocean communicates with the atmosphere through a network of currents termed the meridional overturning circulation. Chokepoints of communication include upwelling currents across density stratification, maintained by turbulent diapycnal mixing. Decades of observations have revealed that the processes driving mixing exhibit prominent spatio-temporal variability, and are often energised in the proximity of complex topography. In turn, recent theoretical and modelling investigations have shown that the spatial distribution of mixing strongly impacts the ocean state, highlighting an imperative to develop realistic and physically consistent representations of key mixing processes. The generation and breaking of internal (or baroclinic) tides is a primary driver of deep-ocean mixing. Lunisolar tides supply ~1 TW of mechanical energy to global internal tide generation outside of continental shelves, which is approximately half of the $2 \pm 0.6$ TW required to fuel global turbulent dissipation and overturning. Lunisolar tides lose their energy on interacting with major features of the seafloor topography, such as mid-ocean ridges and seamounts, and thereby transfer much of the energy to internal tides. Although the geography of internal tide generation is relatively well understood (as it depends, to first order, on well-known barotropic tidal currents and properties of the seafloor topography), the waves’ subsequent evolution and eventual fate are highly uncertain. As a result, parameterisations of tidally driven mixing in climate-scale ocean models are poorly constrained, and mechanistic descriptions of the association between mixing and overturning suffer from fundamental knowledge gaps.

Internal tides span a wide range of vertical and horizontal scales, and it is common practice to cast them into a discrete set of normal modes with distinct structures determined by the local stratification. Observations show that low-mode (i.e., large-scale) internal tides are able to propagate over one thousand kilometres from their generation site, such that their breaking may contribute to far-field oceanic background mixing or remote mixing hot spots. In contrast, high-mode (i.e., small-scale) internal tides are prone to direct breaking, often triggered by wave-wave interactions, and thus drive mixing in the near field of their generation site. The dichotomous fate of low-mode and high-mode waves calls for quantification of the modal partitioning of internal tide generation. Critically, this modal partitioning is directly linked to the parameter $q$, the fraction of locally dissipated tidal energy to local barotropic-to-baroclinic tidal energy conversion. This parameter is a cornerstone of parameterisations of tidal mixing used in state-of-the-art climate-scale ocean models, such as the Community Climate System Model version 4 (CCSM4) and the Nucleus for European Modelling of the Ocean (NEMO). In these models, $q$ adopts a constant value of $1/3$, although the potential for significant spatial variability in $q$ is acknowledged by several studies.

In this paper, we present an estimate of the modal partitioning of global internal tide generation with a resolution of up to 50 modes, and show that its predictions are consistent with available observations of tidal energy conversion, radiation and mixing. We demonstrate that the generation of very high ($>10$) modes accounts for a remarkably large fraction (27%) of all tidal energy conversion. Contrary to current views, reflected in parameterisations of tidal mixing, near-field mixing, associated with locally generated high-mode internal tides, dominates tidal mixing on a global scale (>50%) and exhibits a strong geographical variability: the parameter $q$ is widely distributed across values from 0 to 1. These findings have important implications for the representation of deep-ocean mixing and overturning in climate-scale ocean models, which we discuss.
mode-1 energy flux divergence, \((\nabla \cdot F_{M_1}^1)^+\), also estimated from satellite altimetric data\(^{27}\) (see Methods). \((\nabla \cdot F_{M_1}^1)^+\) quantifies the rate of generation of mode-1 internal tides. These altimetry-based data sets enable us to define regional and global budgets of the M\(_2\) tidal energy, and to validate the predictions of our semi-analytical model (Fig. 1). All terms are integrated for seafloor depths larger than 700 m, in order to exclude shallow topography where the supercritical-slope correction is important (see Supplementary Fig. 1).

The correspondence between observational estimates and our model’s predictions is notable and enables, for the first time, to accurately depict a budget for the energy lost by the barotropic tide, when decomposed into various basins and various contributing components. First, the bulk of the energy lost by the M\(_2\) barotropic tide is found to be converted into internal tides (Fig. 1). All terms are integrated for sea floor depths larger than 700 m, in order to exclude shallow topography where the supercritical-slope correction is important (see Supplementary Fig. 1).

The geographical patterns of \(D_{M_1}\) globally (692 GW vs. 853 ± 171 GW). The contribution of abyssal hills is crucial to close the budget of barotropic tide dissipation, as it represents 12% of the conversion, globally. Note that the marginally significant difference between \(D_{M_1}\) and \(E_{M_1}^-\) in the Atlantic basin, suggestive of missing conversion, may be attributable to under-represented conversion by abyssal hills\(^{25}\). The geographical patterns of \(D_{M_1}\) and \(E_{M_1}^-\) match throughout the global ocean (see Supplementary Note 2 and Supplementary Fig. 2), and reveal that M\(_2\) tidal energy conversion is amplified over mid-ocean ridges, seamounts, and continental shelf breaks (Fig. 2a, b).

Second, there is a close agreement between our model’s predictions (\(E_{M_1}^-\)) and observational estimates ((\(\nabla \cdot F_{M_1}^1\))^+) of the rate of generation of M\(_2\) mode-1 internal tides, both globally and for each of the major ocean basins (Fig. 1). Mode 1 only accounts for 29% of M\(_2\) tidal energy conversion on a global scale. The relative importance of mode-1 is lower in the Atlantic and Indian basins, where mode-1 contributes 21 and 23% of all M\(_2\) tidal energy conversion, but is higher in the Pacific basin, where the fraction of mode-1 conversion is 35%. The enhanced generation of mode-1 internal tides in the Pacific Ocean stems from the basin’s comparative abundance of steep ridges and seamounts, which are conducive to the generation of low-mode baroclinic tides. Hot spots of mode-1 generation are co-located in \(E_{M_1}^-\) and \((\nabla \cdot F_{M_1}^1)^+\) (Fig. 2c, d; Supplementary Note 3 and Supplementary Fig. 3); prominent sites include the Canary Islands, the Atlantic-Meteor Seamount complex, the Iberian shelf break and the Walvis Ridge in the Atlantic Ocean; the northern and southern edges of Madagascar in the Indian Ocean; and the Hawaiian and Polynesian Ridges, the Galápagos archipelago, the Tonga-Kermadec Ridge (north of New Zealand) and the Tasman Sea shelf break in the Pacific Ocean. Other likely sites of important M\(_2\) mode-1 internal tide generation south of 40°S, such as the Kerguelen Plateau, could not be resolved in the observational data set due to contamination of the tidal signals by the region’s energetic mesoscale eddy field. All in all, both our model and the observations indicate that the bulk (71–82%) of M\(_2\) tidal energy conversion occurs in modes higher than 1. This result challenges the widespread view that mode 1 overwhelms tidal energy fluxes\(^{26}\).

The robustness of our model is further endorsed by two independent calculations of the modal partitioning of internal tide generation. Falahat et al.\(^{23}\) used a different approach to ours, but based on the same assumptions, to compute the M\(_2\) tidal energy conversion for the first 10 modes. Their modal distribution closely matches ours for this subset of modes (Fig. 3), with a global conversion into modes 1–10 (integrated up to 700 m) of 518 GW vs. 506 GW. Our model has slightly more energy in modes 6–10, which could be attributed to the better-resolved bathymetry dataset used (SRTM30-PLUS vs. ETOPO2) and the upgraded barotropic tide model used to derive barotropic tidal

\[\text{Fig. 2} \text{ Geography of energy lost by the semidiurnal } M_2 \text{ barotropic tide and converted into internal tides. } a \text{ Energy lost by the } M_2 \text{ barotropic tide, } D_{M_1}, \text{ computed from TPXO8}^{35,} \text{ and } b \text{ barotropic-to-baroclinic tide energy conversion from the semi-analytical model, } E_{M_1}^-\text{. } c \text{ Positive part of the divergence of } M_2 \text{ mode-1 horizontal energy flux } (\nabla \cdot F_{M_1}^1)^+ \text{ derived from satellite altimetry}^{27} \text{ (areas where the mesoscale activity is too strong to recover the internal tide signal are masked in dark grey). and } d \text{ barotropic-to-baroclinic tide energy conversion into mode 1 from the model, } E_{M_1}^-\text{. Areas shallower than 700 m are shown in dark grey.}\]
curren ts (TPXO8 vs. TPXO6.2). Our estimate for modes 1–5 also compares well to the internal tide generation diagnosed in a state-of-the-art global numerical simulation (Fig. 3) at a horizontal resolution of 4 km using the primitive-equation model HYCOM (see Methods). Modes higher than ~4 are only partially resolved in HYCOM as this model cannot adequately represent the horizontal and vertical internal wave lengths. While the consistency between our predictions and these independent estimates is reassuring, our results highlight that modes higher than 10 is hitherto unresolved, account for a large fraction of the total energy conversion. In the deep ocean29, the missing energy sink must be attributed to the HYCOM simulation does not resolve modes >5.

Geographical variability of modal content. The geographical variability of the modal partitioning of M2 tidal energy conversion is illustrated in Fig. 4. Continental shelf breaks, steep ridges and isolated seamounts stand out as preferential locations for mode-1 internal tide generation (Fig. 4a). In contrast, wide ridge systems, such as the Mid-Atlantic Ridge and the East Pacific Rise, systematically display a peak in the energy conversion continuum around modes 2–5. In the deep regions of the Pacific, the most energetic modes are often ≥5.

Although mode 1 is the most energetic mode on a global scale (Fig. 3), its fractional contribution to the total conversion, $E_{M2}^{1}/E_{M2}^{\infty}$, exhibits pronounced geographical variability (Fig. 4b). Over continental shelf breaks and steep ridges, mode 1 can account for over 50% of the total M2 tidal energy conversion. For example, in the Hawaiian Ridge system, mode 1 contributes between 40 and 60% of the total conversion, in the range of the ratios estimated from observations30 and regional numerical simulations31. However, over most of the global ocean, mode 1 accounts for <30% of the M2 tidal energy conversion. Specifically, in wide regions of strong conversion such as the Mid-Atlantic Ridge and the East Pacific Rise, mode 1 contributes less than 10% of the total conversion. Considering that mode 1 may be the only mode capable of propagating far (>1000 km) from its generation site23,32–34, this modal partitioning of conversion suggests that most of the internal tide energy sourced in these regions dissipates within a short distance of generation sites.

**Implications for near-field dissipation.** Areas where strong tidal energy conversion occurs span very different topographic structures, which affect the modal content of locally generated internal tides. Thus, strong geographical variability of near-field dissipation is expected, with high (small) rates where high (low) modes are preferentially generated. Here, we propose a new approach to assess near-field dissipation driven by the breaking of locally generated, high-mode internal tides, which can be used to construct parameterisations of near-field mixing in ocean models (see Discussion). Key to the approach is the definition of a critical mode $n$ above which all modes are assumed to dissipate locally, i.e., within the grid point where conversion occurs. In turn, modes $<n$ can propagate away and dissipate in the far field. The rate of near-field tidal dissipation is thus defined as $E_n^\text{att}$ (see Fig. 33 in Olbers35), among the range of processes that may trigger a forward cascade and dissipation of internal tide energy, we consider only the dominant mechanism, i.e., wave-wave interactions32, which renders our estimate of near-field dissipation conservative. We take the attenuation time scale $\tau_n$ of mode $n$ associated with wave-wave interactions to be proportional to $1/n^2$ (see Fig. 33 in Olbers35), which yields an attenuation length scale for that mode $L_n = c_n/\tau_n$ proportional to $1/n^3$, since the group velocity $c_n$ is proportional to $1/n$. Consequently, $L_n = L_1/n^3$. Using numerical simulations and in situ data from a mooring array aligned with an internal tide beam emanating from the Hawaiian Ridge36, we estimate the characteristic attenuation length scale of mode 1, $L_1$, to be between 700 and 1300 km. Although $L_1$ is expected to vary geographically, depending notably on mesoscale activity and topographic scattering, we find that the critical mode number is weakly sensitive on $L_1$ (see Supplementary Note 4 and Supplementary Figs. 4 and 5). On our global 1/2°-grid, mode 4 is found...
to be the critical mode. Although this method leads to a critical mode that is grid-size-dependent by construction, 1/2° is typical of climate-scale ocean models, and the critical mode can be adjusted to fit different grid sizes. Note that this estimate of near-field dissipation does not account for local breaking of low-mode internal waves occurring at steep ridges, e.g., through lee-wave radiation mechanisms37,38 or direct shear instability39, reinforcing the conservatism of our approach.

The estimated rate of near-field dissipation may be used to quantify q, the fraction of locally dissipated energy to local tidal energy conversion. The definition \( q = E_{M_2}^{4-\infty}/E_{M_2}^{1-\infty} \) is adopted here. The geographical structure of q reflects the spatial variability in the properties of seafloor topography (Fig. 5). Where high-mode internal tide generation is substantial, e.g., over the Mid-Atlantic Ridge and the East Pacific Rise, q is high and reaches values in the range 0.8–1.0. In such regions, the contribution of abyssal hills is critical to weight the conversion towards high modes and reach high q values. In contrast, where low-modes are preferentially generated, e.g., the Hawaiian Islands and other Pacific archipelagos, q displays smaller values of 0.3–0.5. The global-ocean probability density functions of seafloor area and M_2 tidal energy conversion as a function of q (Fig. 5-inset) quantify the geographically variable significance of near-field dissipation. Although half of the global conversion occurs in regions where 0.35 < q < 0.62 (25th and 75th percentiles), half of the seafloor area features 0.45 < q < 0.77 (25th and 75th percentiles). Hence, viewed overall, our conservative, semi-analytical estimate of q highlights the strong spatial variability of near-field dissipation, and shows that, on average, q greatly exceeds the value of 1/3 generally assumed to date.

**In situ observational estimates of turbulent dissipation.** Our model reveals that the generation of energetic high-mode internal tides is widespread across the global ocean. These high modes are characterised by a small group speed and a high vertical shear, which make them prone to breaking close to their generation site. We therefore expect a close relationship between the predicted near-field dissipation of internal tides and the in situ dissipation of turbulent kinetic energy. To evaluate this relationship, we compared our theoretical estimate of near-field dissipation for the eight principal tidal constituents, i.e., \( E_{M_2}^{4-\infty} \) (see Methods), to in situ estimates of turbulent energy dissipation from a finescale parameterisation applied to hydrographic measurements9 and from microstructure observations8. Regions where the mean kinetic energy or the eddy kinetic energy are elevated (>200 cm^2 s^-2, visually chosen to discard western boundary currents, the Antarctic Circumpolar Current and equatorial zonal jets) are excluded from the comparison, since non-tidal processes (e.g., submesoscale instabilities40,41) are expected to play an important role in dissipation there (see Methods).

The two-dimensional histogram of finescale dissipation vs. predicted near-field dissipation (Fig. 6) shows that there is a strong relationship between the two variables that approaches 1:1 whenever the conversion is significant (>5 x 10^-4 W m^-2, typical lower bound in regions where tidal energy conversion occurs24).

Indeed, \( r^2 = 0.96 \) for the linear regression on data binned in 0.1 log intervals. For smaller rates of conversion (shadowed area), observed dissipation exceeds the theoretical estimate, which suggests that turbulence in those areas is predominantly fuelled by other local (e.g., wind-driven) or non-local (e.g., far-field dissipation of low-mode internal tides11) processes. Note that in regions of rough topography, the finescale parameterisation may lose accuracy42 and so could be unsuitable to examine near-field dissipation.

Microstructure profilers measure microscale turbulence, and thus provide the most reliable estimates of the rate of turbulent dissipation. We consider a subset of the microstructure-derived dissipation estimates gathered by Waterhouse et al.8 relevant to tidally induced mixing, and augmented with the more recent RidgeMix22 and DoMORE43 data sets collected over the northern and southern Mid-Atlantic Ridge, respectively. Only stations where the predicted tidal conversion exceeds 5 x 10^-4 W m^-2 are examined (Fig. 6). Pictograms and associated error bars indicate the mean and standard deviation values for each cruise data set. Error bars thus encode the spatial (horizontal and vertical error bars) and temporal (vertical error bars) variability of turbulent dissipation for each expedition, where some of the variability likely stems from spring-neap cycle biases in sampling22 and other low-frequency, non-tidal processes. This scatter plot highlights the close connection between tidal energy conversion into high modes and local energy dissipation, as the linear...
climate-scale ocean models. Such parameterisations are constructed from maps of barotropic-to-baroclinic tidal energy conversion for the eight principal tidal constituents. A fraction of the energy conversion, usually taken to be uniform and equal to 1/3, is assumed to fuel dissipation within the local water column. This dissipation is then distributed vertically, following an exponential decay from the seafloor upward. In the following, we ignore the vertical distribution within the water column, and focus on the maps of energy conversion providing local dissipation. The NEMO model\(^1\) uses 1/3 of the global estimate of energy conversion by Nycander\(^4\), and is hereafter denoted \(E_{\text{NEMO}}\). The CCSM4 model\(^1\) uses the parameterisation of energy conversion of Jayne and St. Laurent\(^5\), re-scaled as in Jayne\(^6\) to produce 1 TW of dissipation below 1000 m, and then multiplied by 1/3. It is hereafter denoted \(E_{\text{CCSM}}\).

The three estimates of local dissipation, \(E_{\text{all}}\), \(E_{\text{NEMO}}\) and \(E_{\text{CCSM}}\), produce 606, 413, and 482 GW of energy dissipation at seafloor depths exceeding 500 m, respectively. At seafloor depths shallower than 2500 m, \(E_{\text{all}}\) and \(E_{\text{CCSM}}\) are very similar (391 vs. 381 GW), but \(E_{\text{NEMO}}\) is weaker (261 GW). Differences become more pronounced at seafloor depths deeper than 2500 m, where \(E_{\text{all}}\) represents 215 GW of dissipation, which is 41\% larger than \(E_{\text{NEMO}}\) (152 GW) and 113\% larger than \(E_{\text{CCSM}}\) (101 GW). The larger dissipation below 2500 m is consistent with large \(q\) values found over abyssal topography (Fig. 5).

The map of \(E_{\text{all}}\) illustrates the near-field dissipation hotspots, such as mid-ocean ridges featuring rough topography (Fig. 7b). The ratio of our estimate to the others highlights two important differences (Fig. 7c, d). In regions of rough topography, our estimate gives higher levels of dissipation because of the high-mode internal tide generation that is absent from \(E_{\text{NEMO}}\) and \(E_{\text{CCSM}}\). In contrast, over steep ridges and seamounts, mostly in the Pacific basin, dissipation is comparatively weaker than for \(E_{\text{NEMO}}\) and \(E_{\text{CCSM}}\) because modes 1–3 are excluded from our estimate. We do not expect strong dissipation—relative to conversion—at the latter generation hot spots, but rather a redistribution by low modes contributing to far-field dissipation.

The patterns and magnitudes of near-field dissipation estimated in the present work thus differ substantially from those implied by current parameterisations. Implications are manifold. First, our mode-partitioned internal tide generation estimate may serve to improve the representation of wave drag, i.e., the energy extracted locally from the barotropic tide, in barotropic tide models\(^45\) and in climate-scale ocean models that include tidal forcing\(^46\). Notably, our estimate takes into account the local properties of seafloor topography, and should thereby reduce known geographical biases in barotropic tide models\(^45\). Second, our map of \(E_{\text{all}}\) can provide the power input to the parameterisation of near-field internal tide-driven mixing. Its use in place of preceding maps is expected to improve the representation of deep-ocean mixing in ocean models, potentially improving the simulated overturning circulation by reconciling strong abyssal transports with slow pycnocline mixing\(^47\) (Fig. 7a). Overall, our revised estimate of internal tide-driven dissipation will help narrow down unknowns in the rates and energy pathways of deep-ocean mixing, and represents a significant step toward the closure of oceanic energy and diapycnal mixing budgets in observations and models.

**Methods**

**Semi-analytical model of tidal energy conversion.** The barotropic-to-baroclinic tide energy conversion model was formulated by Bell\(^28\), and is based on two main assumptions that enable derivation of a linear theory. First, the topographic slope, \(|Vh|\), is assumed to be smaller than the slope of a radiated internal wave beam, \((\omega^2 - f^2)/(N_b^2 - \omega^2)^{1/2}\), where \(\omega\) is the tidal frequency, \(f\) is the Coriolis frequency and \(N_b\) is the buoyancy frequency near the seafloor. The ratio of the
topographic slope to the slope of a radiated beam defines the steepness parameter:

$$y = \left| \frac{\nabla h}{(\omega^2 - f^2)/\left(N_0^2 - \omega^2\right)} \right|^{1/2}. \quad \text{(1)}$$

When $y < 1$ ($y > 1$), the topography is referred to as subcritical (supercritical). Second, the tidal excursion, $u_b/u_s$, where $u_b$ is the barotropic tide velocity, is assumed to be small compared to the topographic scale $1/k$, where $k$ is a characteristic wavenumber of the underlying topography. In the deep ocean, i.e., excluding continental shelves, the major topographic structures generating internal tides are mid-ocean ridges. The assumptions of subcritical topography and small tidal excursion are valid on most of the areas covered by these structures, due to weak barotropic tidal currents $|u_b| = O(1) \text{ cm s}^{-1}$ and weak stratification that allows beams to propagate in a direction close to the vertical.

We used St. Laurent and Garrett\'s\textsuperscript{22} formulation of tidal energy conversion, $E_{\nu}$, at a fundamental tidal frequency $\nu$:

$$E_{\nu}(K, \theta) = \frac{1}{4} \rho_o \left( \frac{\omega_2^2 - \omega_0^2}{\omega_2^2 - \omega_1^2} \right)^2 \left( \cos^2 \theta + \sin^2 \theta \right) K \phi(K, \theta). \quad \text{(2)}$$

In this equation, $N_0$ is the buoyancy frequency close to the bottom computed from the World Ocean Atlas 2013 (WOA13\textsuperscript{[4]}) $u_b$ is the barotropic tidal velocity amplitude from TPXO8\textsuperscript{[18]}, in the direction of the semimajor (semiminor) axis of the tidal ellipse $(x, y)$ coordinate system; $K = (k_x^2 + k_y^2)^{1/2}$ is the total horizontal wavenumber, with $k_x$ and $k_y$ being the horizontal wavenumbers in the $(x, y)$ coordinate system; and $\theta = \arctan(k_y/k_x)$. The two-dimensional power spectrum of topography, $\phi$, is computed from the Shuttle Radar Topography Mission dataset (SRTM30 PLUS\textsuperscript{[10]}) SRTM30_PLUS is a global bathymetry dataset at a 30-s resolution based on the 1-min Smith and Sandwell bathymetry, and incorporates higher-resolution data from ship soundings wherever available. $\phi$ is normalised to satisfy \( \int_{x_1}^{x_2} \int_{y_1}^{y_2} \phi(K, \theta) K \, dK \, d\theta = \overline{H^2} \), where $\overline{H^2}$ is the mean square height of topography.

The equivalent wavenumber of mode $j$ is

$$K_j = \frac{j \pi (\omega_2 - f)^{1/2}}{N_0 b}. \quad \text{(3)}$$

$N_0$ and $b$ are parameters of an exponential fit to the buoyancy frequency $N = N_0 \exp(z/b)$. This enables computation of the energy flux into mode $j$ as

$$E_{\nu}^j = \int_0^{2\pi} \int_{K_j - \Delta K/2}^{K_j + \Delta K/2} E_{\nu}(K, \theta) K \, dK \, d\theta \quad (\text{W m}^{-2}). \quad \text{(4)}$$

where $\delta K = K_2 - K_1$. The total energy flux is then

$$E_\nu = \int_0^\infty \int_{K_1}^{K_2} E_{\nu}(K, \theta) K \, dK \, d\theta \quad (\text{W m}^{-2}), \quad \text{(5)}$$

where the lower boundary of integration in wavenumber space is the mode-1 equivalent wavenumber, $K_1$, to take into account the finite depth of the ocean.

We computed $E_\nu$ for $\omega \in [M_2, S_2, K_1]$ on a global grid of $1/2^\circ$ resolution. A supercritical-slope correction was made a posteriori (see Supplementary Note 1). We only considered the points where the bathymetry is deeper than 500 m. At shallower ocean depths, topographic slopes are more likely to be supercritical due to enhanced stratification, and tidal currents are stronger due to mass continuity, hence potentially violating the small tidal excursion assumption.

**Barotropic tide energy dissipation.** The dissipation rate of the barotropic tide, $D_{\nu}$, at the tidal frequency $\omega$ can be computed as\textsuperscript{39}

$$D_{\nu} = W - \nabla \cdot \mathbf{P} \quad (\text{W m}^{-2}), \quad \text{(6)}$$

where $W$ is the work done by the barotropic tide, and $\mathbf{P}$ is the barotropic tide energy flux. $\mathbf{P}$ is defined as

$$\mathbf{P} = \rho_0 \bar{g} (\mathbf{U} \cdot \nabla), \quad \text{(7)}$$

where $\bar{g}$ is the tidal elevation, and $\mathbf{U}$ is the barotropic tide volume transport, both extracted from TPXO8. $W$ is defined as

$$W = \rho_0 \bar{g} \left( \mathbf{U} \cdot \nabla (\bar{e}_t + \bar{e}_{\text{int}}) \right), \quad \text{(8)}$$

where $\bar{e}_t$ is the equilibrium tidal elevation, and $\bar{e}_{\text{int}}$ is the tidal elevation induced by the tide’s self-attraction and loading\textsuperscript{33}.

**Mode-1 $M_2$ energy fluxes from satellite altimetry.** Mode-1 $M_2$ internal-tide horizontal energy flux at a horizontal resolution of $1/10^\circ$ from Zhao et al.\textsuperscript{32} was used in this study to quantify the generation of $M_2$ internal tides. A two-dimensional plane wave fit method is applied to extract internal tides from satellite SSH, and perform a modal decomposition that enables inference of mode-1 internal tide pressure from SSH. Assuming that the energy partition between potential and kinetic energy components depends only on latitude and tidal frequency, the internal tide velocity is also estimated from SSH. Finally, the vertically integrated horizontal energy flux, $\mathbf{F}_{\text{int}}$, is computed. Positive divergence of the horizontal energy flux, denoted as $\left( \mathbf{V} \cdot \mathbf{F}_{\text{int}} \right)^+$ in the article, indicates regions of mode-1 internal tide generation\textsuperscript{32}.

![Fig. 7 Comparison of proposed and currently used estimates of near-field tidal mixing. a Distribution of energy dissipation as a function of seafloor depth for the three estimates: (black) our proposed estimate, $E_{\nu}^j$; (dark grey) $E_{\nu}^{NEMO}$, based on Nycander’s estimate of energy conversion and used in the NEMO model; and (light grey) $E_{\nu}^{CCSM}$, based on Jayne and St-Laurent’s estimate and used in the CCSM4 model. Maps of b $E_{\nu}^j$, c $E_{\nu}^{NEMO}$, and d $E_{\nu}^{CCSM}$.](Image)
Global HYCOM simulation. HYCOM (Hybrid Coordinate Ocean Model) is the operational ocean forecast model used by the United States Navy\cite{32}. The simulation considered in this study was run with realistic atmospheric forcing from the NAVy Global Environmental Model (NAVGEM)\cite{33} and astronomical tidal forcing. The model was run in a forward (non-data- assimilative) mode at 1/25 degree (4 km) nominal horizontal resolution, with 41 layers in the vertical, using a hybrid vertical coordinate that is isopycnal in the open ocean, uses z-layers in the mixed layer, and transitions to terrain-following in shallow water. Hourly 3-d fields were saved from September 2016; 15 days of this period were analysed for this paper. Data were interpolated to 25-m depth intervals in the vertical and harmonic fits were applied to extract the M2 component of the baroclinic velocities and potential density at each depth level. Vertical normal modes were computed from the time-averaged stratification profile by solving the Sturm-Liouville problem. The 4 km model resolution effectively limits the resolved modes to the first 5 baroclinic modes. Modal barotropic-to-baroclinic conversion values were computed from the modol perturbation pressure amplitudes, bathymetry, and barotropic velocity\cite{87}.

Modal barotropic-to-baroclinic tidal energy conversion model is available upon request.

References

1. Polzin, K., Tooze, J., Ledwell, J. & Schmitt, R. Spatial variability of turbulent mixing in the abyssal ocean. Science 276, 91–96 (1997).
2. Jayne, S. R. The impact of abyssal mixing parameterizations in an ocean general circulation model. J. Phys. Oceanogr. 39, 1756–1775 (2009).
3. de Lavergne, C., Madec, G., Le Sommer, J., Nurser, A. G. & Naveira Garabato, A. C. On the consumption of Antarctic Bottom Water in the abyssal ocean. J. Phys. Oceanogr. 46, 635–661 (2016).
4. Melet, A., Legg, S. & Hallberg, R. Climatic impacts of parameterized local and remote tidal mixing. J. Clim. 29, 3473–3500 (2016).
5. Munk, W. & Wunsch, C. Abyssal recipes II: energetics of tidal and wind mixing. Deep-Sea Res. I 45, 1977–2010 (1998).
6. Ferreira, R. & Wunsch, C. Ocean circulation kinetic energy: reservoirs, sources, and sinks. Annu. Rev. Fluid Mech. 41, 253 (2009).
7. MacKinnon, J. A. et al. Climate process team on internal-wave driven ocean mixing. Bull. Am. Meteor. Soc. 98, 2429–2454 (2017).
8. Waterhouse, A. F. et al. Global patterns of diapycnal mixing from measurements of the turbulent dissipation rate. J. Phys. Oceanogr. 44, 1854–1872 (2014).
9. Kunze, E. Internal-wave-driven mixing: Global geography and budgets. J. Phys. Oceanogr. 47, 1325–1345 (2017).
10. Garrett, C. & Kunze, E. Internal tide generation in the deep ocean. Annu. Rev. Fluid Mech. 39, 57–87 (2007).
11. Alford, M. H. Redistribution of energy available for ocean mixing by long- range propagation of internal waves. Nature 423, 159–162 (2003).
12. Nikurashin, M. & Legg, S. A mechanism for local dissipation of internal tides generated at rough topography. J. Phys. Oceanogr. 41, 378–395 (2011).
13. St Laurent, L., Simmons, H. & Jayne, S. Estimating tidally driven mixing in the deep ocean. Geophys. Res. Lett. 29, 211–214 (2002).
14. Danabasoglu, G. et al. The CCSM4 ocean component. J. Clim. 25, 1361–1389 (2012).
15. Madec, G. et al. NEMO ocean engine. Tech. Rep. (2015).
16. St Laurent, L. & Nash, J. An examination of the radiative and dissipative properties of deep ocean internal tides. Deep-Sea Res. II 51, 3029–3042 (2004).
17. Falahat, S., Nycander, J., Roquet, F., Thurnherr, A. M. & Hibiya, T. Comparison of calculated energy flux of internal tides with microstructure measurements. Tellus A 66, 23240 (2014).
18. Lefauve, A., Muller, C. & Melet, A. A three-dimensional map of tidal dissipation over abyssal hills. J. Geophys. Res. Oceans 120, 4760–4777 (2015).
19. Bell, T. Lee waves in stratified flows with simple harmonic time dependence. J. Fluid Mech. 67, 705–722 (1975).
20. Bell, T. Topographically generated internal waves in the open ocean. J. Geophys. Res. 80, 320–327 (1975).
21. St Laurent, L. & Garrett, C. The role of internal tides in mixing the deep ocean. J. Phys. Oceanogr. 32, 2882–2899 (2002).
22. Vic, C. et al. The lifecycle of semidiurnal internal tides over the northern Mid-Atlantic Ridge. J. Phys. Oceanogr. 48, 61–80 (2018).
23. Falahat, S., Nycander, J., Roquet, F. & Zarroug, M. Global calculation of tidal energy conversion into vertical normal modes. J. Phys. Oceanogr. 44, 3225–3244 (2014).
24. Nycander, J. Generation of internal waves in the deep ocean by tides. J. Geophys. Res. 110, C01036 (2005).
25. Melet, A. et al. Internal tide generation by abyssal hills using analytical theory. J. Phys. Geophys. Res. 118, 6303–6318 (2013).
26. Egbert, G. D. & Ray, R. D. Semi-diurnal and diurnal tidal dissipation from TOPEX/Poseidon altimetry. Geophys. Res. Lett. 30, 1907 (2003).
27. Zhao, Z., Alford, M. H., Girton, J. B., Rainville, L. & Simmons, H. L. Global observations of open-ocean mode 1 M2 internal tides. J. Phys. Oceanogr. 46, 1657–1684 (2016).
28. Ray, R. D. & Cartwright, D. E. Estimates of internal tide energy fluxes from TOPEX/Poseidon altimetry: Central North Pacific. Geophys. Res. Lett. 28, 1259–1262 (2001).
29. Buijsman, M. C. et al. Impact of parameterized internal wave drag on the semidiurnal energy balance in a global ocean circulation model. J. Phys. Oceanogr. 46, 1399–1414 (2016).
30. Rudnick, D. L. et al. From tides to mixing along the Hawaiian Ridge. Science 301, 353–357 (2003).
31. Merrifield, M. A. & Holloway, P. E. Model estimates of M2 internal tide energetics at the Hawaiian Ridge. J. Geophys. Res. 107, 5–15–5–12 (2002).
32. Rainville, L. & Pinkel, R. Propagation of low-mode internal waves through the ocean. J. Phys. Oceanogr. 36, 1220–1236 (2006).
33. Alford, M. H. & Zhao, Z. Global patterns of low-mode internal-wave propagation. Part I: Energy and energy flux. J. Phys. Oceanogr. 37, 1829–1848 (2007).
34. Zhao, Z., Alford, M. H., MacKinnon, J. A. & Pinkel, R. Long-range propagation of the semidiurnal internal tide from the Hawaiian Ridge. J. Phys. Oceanogr. 40, 713–736 (2010).
35. Olbers, D. J. Models of the oceanic internal wave field. Rev. Geophys. 21, 1567–1606 (1983).
36. Wurz, J. K. et al. Semidiurnal internal tide energy fluxes and their variability in a Global Ocean Model and moored observations. J. Geophys. Res. Oceans 122, 1882–1900 (2017).
37. Legg, S. & Klymak, J. Internal hydraulic jumps and overturning generated by tidal flow over a tall steep ridge. *J. Phys. Oceanogr.* **38**, 1949–1964 (2008).
38. Klymak, J. M., Pinkel, R. & Rainville, L. Direct breaking of the internal tide near topography: Kaena Ridge, Hawaii. *J. Phys. Oceanogr.* **38**, 380–399 (2008).
39. Van Haren, H. & Gostiaux, L. A deep-ocean Kelvin-Helmholtz billow train. *Geophys. Res. Lett.* **37**, L03605 (2010).
40. D’Asaro, E., Lee, C., Rainville, L., Thomas, L. & Harcourt, R. Enhanced turbulence and energy dissipation at ocean fronts. *Science* **332**, 318–322 (2011).
41. Gula, J., Molemaker, M. J. & McWilliams, J. C. Topographic generation of submesoscale centrifugal instability and energy dissipation. *Nat. Commun.* **7**, 12811 (2016).
42. Liang, C.-R., Shang, X.-D., Qi, Y.-F., Chen, G.-Y. & Yu, L.-H. Assessment of fine-scale parameterizations at low latitudes of the North Pacific. *Sci. Rep.* **8**, 10 (2018).
43. Clément, L., Thurnherr, A. M. & St. Laurent, L. C. Turbulent mixing in a deep fracture zone on the Mid-Atlantic Ridge. *J. Phys. Oceanogr.* **47**, 1873–1896 (2017).
44. Jayne, S. R. & St Laurent, L. C. Parameterizing tidal dissipation over rough topography. *Geophys. Res. Lett.* **28**, 811–814 (2001).
45. Egbert, G. D., Ray, R. D. & Bills, B. G. Numerical modeling of the global semi-diurnal tide in the present day and in the last glacial maximum. *J. Geophys. Res. Oceans* **109**, C03003 (2004).
46. Arbic, B. K., Garner, S. T., Hallberg, R. W. & Simmons, H. L. The accuracy of surface elevations in forward global barotropic and baroclinic tide models. *Deep-Sea Res. II* **51**, 3069–3101 (2004).
47. de Lavergne, C., Madec, G., Roquet, F., Holmes, R. & McDougall, T. Abyssal ocean overturning shaped by seafloor distribution. *Nature* **551**, 181 (2017).
48. Locarnini, R. et al. World Ocean Atlas 2013, Vol. 1: Temperature. NOAA Atlas NESDIS **73**, 40 (2013).
49. Zweng, M. et al. World Ocean Atlas 2013, Vol. 2: Salinity. NOAA Atlas NESDIS **74**, 39 (2013).
50. Egbert, G. D. & Erofeeva, S. Y. Efficient inverse modeling of barotropic ocean tides. *J. Atmos. Ocean. Technol.* **19**, 183–204 (2002).
51. Becker, J. et al. Global bathymetry and elevation data at 30 arc seconds resolution: SRTM30_PLUS. *Mar. Geod.* **32**, 355–371 (2009).
52. Smith, W. & Sandwell, D. Global sea floor topography from satellite altimetry and ship depth soundings. *Science* **277**, 1596–1602 (1997).
53. Egbert, G. & Ray, R. Significant dissipation of tidal energy in the deep ocean inferred from satellite altimeter data. *Nature* **405**, 775–778 (2000).
54. Ray, R. Ocean self-attraction and loading in numerical tidal models. *Mar. Geod.* **21**, 181–192 (1998).
55. Metzger, E. J. et al. US Navy operational global ocean and Arctic ice prediction systems. *Oceanography* **27**, 32–43 (2014).
56. Hogan, T. F. et al. The navy global environmental model. *Oceanography* **27**, 116–125 (2014).
57. Buijsman, M. C. et al. Three-dimensional double-ridge internal tide resonance in Luzon Strait. *J. Phys. Oceanogr.* **44**, 850–869 (2014).
58. de Lavergne, C. et al. Toward global maps of internal tide energy sinks. *Ocean Model.* **137**, 52–75 (2019).
59. de Boyer Montégut, C., Madec, G., Fischer, A. S., Lazar, A. & Iudicone, D. Mixed layer depth over the global ocean: An examination of profile data and a profile-based climatology. *J. Geophys. Res. Oceans* **109**, C12003 (2004).
60. Falahat, S. et al. Global estimates of internal tide generation rates at 1/3° resolution. SEANOE. *https://doi.org/10.58153/58153* (2018).

**Acknowledgements**

We thank Eric Kunze for providing the finestructure parameterisation of dissipation. C.V. and A.C.N.G. were supported by the U.K. Natural Environment Research Council through Grant NE/L004216/1. A.C.N.G. further acknowledges the support of the Royal Society and the Wolfson Foundation. The HYCOM portion of this work was funded by the Office of Naval Research grant N00014-15-1-2288 and National Science Foundation grant OCE1537449. Jay Shriver is acknowledged for performing the HYCOM simulations and making their data available.

**Author contributions**

C.V., A.C.N.G., M.G., and C.d.L. designed the experiments, conducted the analyses and led the writing of the manuscript. A.F.W. provided guidance on the use and interpretation of the microstructure data. Z.Z. provided guidance on the use and interpretation of the satellite-derived energy fluxes. A.M. provided and helped interpreting energy conversion due to abyssal hills. M.C.B. and G.R.S. provided guidance on the use of HYCOM outputs.

**Additional information**

Supplementary Information accompanies this paper at https://doi.org/10.1038/s41467-019-10149-5.

**Competing interests:** The authors declare no competing interests.

Reprints and permission information is available online at http://npg.nature.com/reprintsandpermissions/

**Journal peer review information: Nature Communications** thanks Steven Jayne, Hesam Salehipour and Ali Mashayek for their contribution to the peer review of this work

**Publisher’s note:** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. The images or other third party material in this article are included in the article’s Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the article’s Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit http://creativecommons.org/licenses/by/4.0/.

© The Author(s) 2019