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To cite this version:
Francois Bruno, Jean-Baptiste Laudereau, Max Lesaffre, Nicolas Verrier, Michael Atlan. Phase-sensitive narrowband heterodyne holography. 2013. hal-00782727v2

HAL Id: hal-00782727
https://hal.science/hal-00782727v2
Preprint submitted on 16 Jan 2014

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Phase-sensitive narrowband heterodyne holography

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We report on amplitude and phase imaging of out-of-plane sinusoidal surface vibration at nanometer scales with a heterodyne holographic interferometer. The originality of the proposed method is to make use of a multiplexed local oscillator to address several optical sidebands into the temporal bandwidth of a sensor array. This process is called coherent frequency-division multiplexing. It enables simultaneous recording and pixel-to-pixel division of sideband holograms, which permits quantitative wide-field mapping of optical phase modulation depths. Additionally, a linear frequency chirp ensures the retrieval of the local mechanical phase shift of the vibration with respect to the excitation signal. The proposed approach is validated by quantitative motion characterization of the lamellophone of a musical box, behaving as a group of harmonic oscillators, under weak sinusoidal excitation. Images of the vibration amplitude versus excitation frequency show the resonance of the nanometric flexural response of one individual cantilever, at which a phase hop is measured.

Imaging nanometric optical path length modulations is of interest in non-destructive testing of micro electromechanical systems [1–4]. Among the approaches used for single-point vibration spectra measurements, laser Doppler schemes are commonly found; they enable non-contact out-of-plane vibration monitoring [4, 5]. In these measurement schemes, the resolution of the minimum measurable vibration amplitude is limited by the detection sensitivity [2, 3, 6, 7, 8]. These methods exhibit high reliability for wideband [10–13] and narrowband [4, 6, 8] measurements. Narrowband measurements facilitate high frequency monitoring without the need for specialized electronics [3, 6], while wideband measurements allow for transient signal analysis [11]. Nevertheless, imaging is a tedious and time-consuming process because laser probe scanning is required. To circumvent scanning issues, wide-field heterodyne optical detection schemes with dedicated sensor arrays were introduced recently [14, 15]. Another approach involves time-averaged holographic interferometry, which permits high sensitivity measurements [16, 17]. This method enables narrowband measurements of the optical path-length modulation depth when the exposure time of the recorded interferogram is much longer than the vibration period [17, 22, 23]. With this approach, the optical phase retardation of the recorded scattered field beating against a reference optical field can also be exploited for time-resolved (wideband) determination of the object motion [23, 24]. Nevertheless, typical vibration frequencies of interest in non-destructive monitoring are still much higher than camera frame rates, and hence the time-averaging condition holds. In this regime, the phase shift with respect to the excitation signal is usually retrieved from phase-stepped stroboscopic schemes [1, 22, 23]. Quantitative imaging of optical path length modulation and phase retardation in stationary regimes, at the time scale of the frame exposure, may thus find applications.

In this letter, we report on a heterodyne holographic arrangement used for amplitude and phase imaging of optical path length modulation in time-averaged recording conditions, without strobe light. The proposed arrangement consists of a Mach-Zehnder holographic interferometer in an off-axis and frequency-shifting configuration [23, 30], with a multiplexed local oscillator (Fig. 1). Frequency-tunable narrowband detection is achieved in time-averaged heterodyne detection conditions. Time-averaged holograms of a phase-modulated optical field are recorded with an exposure time much longer than the modulation period. Optical heterodyning is performed with a frequency-shifted optical local oscillator, a frequency-conversion process aimed at shifting a given radiofrequency (RF) optical sideband in the sensor bandwidth. Optical local oscillator multiplexing is realized by the coherent addition of RF signals driving an acousto-optic modulator in the reference beam channel. Coherent frequency-division multiplexing is a technique by which the total available bandwidth is divided into non-overlapping frequency sub-bands carrying separate signals. Addressing simultaneously distinct domains of the spectral bandwidth of

FIG. 1: Experimental set-up.
holograms was performed with success for angular \[31\], wavelength \[32\], space-division \[33\], and sideband \[23\] multiplexing schemes. Coherent frequency-division multiplexing in heterodyne holography offers the opportunity to measure complex-valued maps of the RF spectral components of the optical radiation field with accuracy and sensitivity, as long as they can be isolated in sub-bands of the sensor’s temporal bandwidth. In the reported experiment, high-quality factor flexural responses at audio frequencies of a lamellophone (the metallic comb of cantilevers from a musical box) excited in a sympathetic resonance regime are sought. Symphatic vibration is a harmonic phenomenon wherein a vibratory body responds to external excitation in the vicinity of a resonance frequency.

The optical setup used to perform non-destructive testing of the cantilevers’ out-of-plane flexural responses at nanometric scales is sketched in Fig. \[\text{I}\]. It is designed to monitor quantitatively steady-state vibration amplitudes and to detect mechanical phase jumps with respect to the excitation signal, by interferometric detection of an optical field scattered by the lamellophone, referred to as the object field, beating against a reference optical field. The out-of-plane motion of the cantilevers provokes an optical path length modulation of the backscattered object field. Hence the temporal part of the object field \(E\) undergoes a sinusoidal phase modulation \(\phi(t) = 4xz(t)/\lambda\). The equation of the out-of-plane motion \(z(t)\) of a cantilever, modeled as a damped harmonic oscillator of spring constant \(k\), mass \(m\), damping coefficient \(c\), driven sinusoidally by the force \(F(t) = F_0 \sin(\omega t)\) provided by a piezo-electric actuator is

\[
m \frac{\partial^2 z}{\partial t^2} + c \frac{\partial z}{\partial t} + kz = F(t)
\]

We seek a steady-state solution at the excitation frequency with an induced phase change of \(\psi\) with respect to the excitation \(F(t)\), as a result of viscous damping

\[
z(t) = z_0 \sin(\omega t + \psi)
\]

Its amplitude, \(z_0\), is proportional to the driving force

\[
z_0 = \frac{F_0}{m\omega} \left[ \left(2\omega_0\zeta\right)^2 + \frac{1}{\omega^2} \left(\omega_0^2 - \omega^2\right)^2 \right]^{-1/2}
\]

Two intermediate variables were introduced: the angular resonance frequency \(\omega_0\) of the undamped oscillator, and the dimensionless damping ratio \(\zeta\). They satisfy the relationships \(k = m\omega_0^2\) and \(c = 2m\omega_0\zeta\). The phase shift of the sinusoidal response with respect to the driving force is

\[
\psi = \arctan \left( \frac{2\omega_0\zeta}{\omega^2 - \omega_0^2} \right)
\]

The resonance frequencies \(\omega_r = \omega_0 \sqrt{1 - 2\zeta^2}\) of each cantilever are almost equal to the resonant frequencies \(\omega_0\) of the undamped system. The monochromatic optical field of amplitude \(E\), oscillating at the angular frequency \(\omega_l\), backscattered by the object in vibration can be written

\[
E = E \exp \left[ i\omega_l t + i\phi(t) \right]
\]

The phase-modulated field can be decomposed on a basis of Bessel functions of the first kind \(J_n(\phi_0)\), via the Jacobi-Anger identity

\[
E = E \exp(i\omega_l t) \sum_n J_n(\phi_0) \exp \left[ in(\omega t + \psi) \right]
\]

where the quantity

\[
E_n = EN_n(\phi_0) \exp(in\psi)
\]

is the complex weight of the optical sideband of order \(n\), and \(\phi_0 = 4\pi z_0/\lambda\) is the modulation depth of the optical phase of the radiation backscattered by the cantilever. The local amplitude \(z_0\) of the out-of-plane vibration and phase retardation \(\psi\) with respect to the sinusoidal driving force can be derived from the complex weight of two optical sidebands with Eq. (7) and the first-order Taylor developments of \(J_0(\phi_0)\) and \(J_1(\phi_0)\), near \(\phi_0 = 0\), for \(z_0 \ll \lambda/(\Delta \omega_l)\).

\[
\frac{E_1}{E_0} \approx \frac{2\pi}{\lambda} z_0 \exp(i\psi)
\]

The holographic interferometer is used for the detection of RF phase modulation sidebands of an object field \(E\) in reflective geometry, beating against a LO field \(E_{LO}\), as reported in \[23\]. Its purpose is to enable a robust quantitative measurement of the nanometric modulation amplitudes of cantilever resonances, as well as the associated phase shift with respect to the sinusoidal excitation signal. To do so, the adopted strategy is to separate the sensor bandwidth \(-\omega_S/2, \omega_S/2\) into three non-overlapping frequency sub-bands, centered at \(\delta \omega_1, \delta \omega_2,\) and \(\delta \omega_3, each of which is used to carry a separate optical modulation sideband. The LO signal is composed of the sum of three phase-locked RF signals, to yield an optical LO field of the form

\[
E_{LO} = E_{LO} \exp(i\omega_l t) \sum_{n=1}^{3} \alpha_n \exp(i\Delta \omega_n t)
\]

where \(\Delta \omega_n = (n - 2)\omega - \delta \omega_n\) is the frequency shift and \(\alpha_n E_{LO}\) is the complex weight of the LO component of rank \(n = 1, 2, 3\). The positive parameters \(\alpha_n\) are the normalized weights of each LO component; in this experiment \(\alpha_1 = \alpha_2 = \alpha_3 = 1/3\). The LO components are tuned around the optical modulation bands of order \(-1, 0, +1\). Precisely, the LO component of rank \(n\) beats against the optical modulation band of rank \(n - 2\) at the apparent frequency \(\delta \omega_n\), which is set within the camera bandwidth. The sensor array used for detection is an EMCCD camera, (Andor IXON 885+, frame rate \(\omega_S/(2\pi) = 20\) Hz). The main optical radiation field is provided by a doubled Nd:YAG laser (Oxxius SLIM 532, power 100 mW, wavelength \(\lambda = 532\) nm, optical pulsation \(\omega_0\)). Image rendering from the raw interferograms...
be expressed as

\[ H(t) = \sum_{n=1}^{3} E_{n-2} E_{LO}^{*} \alpha_n \exp(i\delta\omega_n t) \]  \hspace{3cm} (11)

where the quantities \( \delta\omega_n \) satisfy \(-\omega_S/2 < \delta\omega_n < \omega_S/2\).

The FFT-spectrum of \( N \) consecutive off-axis holograms

\[ \tilde{H}(\omega_n) = \sum_{p=1}^{N} H(2\pi p/\omega_S) \exp(-2i\pi p/N) \]  \hspace{3cm} (12)

exhibits three peaks at the frequencies \( \delta\omega_1, \delta\omega_2, \) and \( \delta\omega_3 \) (Fig. 3). Their complex values yield holograms \( \tilde{H}_m \) of rank \( m = -1, 0, 1 \), whose magnitude is proportional the modulation depth at the frequency \( \delta\omega_{m+2} \)

\[ \tilde{H}_m = \tilde{H}(\delta\omega_{m+2}) = A E_m \]  \hspace{3cm} (13)

where \( A \propto E_{LO}^{*} \alpha_m \) is a complex constant. Thus, \( \tilde{H}_m \) is a measure of the complex weight \( E_m \). For small-amplitude vibrations, a quantitative map of the local out-of-plane vibration amplitude \( z_0 \) can be assessed from the ratio of the first-order sideband \( \tilde{H}_1 \) and the non-shifted light component \( \tilde{H}_0 \)

\[ z_0 = \frac{\lambda}{2\pi} \left| \tilde{H}_1/\tilde{H}_0 \right| \]  \hspace{3cm} (14)

In the same manner, a map of the local mechanical phase retardation \( \psi \) with respect to the excitation signal can be assessed from \( \tilde{H}_1 \) and \( \tilde{H}_0 \)

\[ \psi - \psi_0 = \text{Arg} \left( \tilde{H}_1/\tilde{H}_0 \right) \]  \hspace{3cm} (15)

where \( \psi_0(t) = \delta\omega_3 t - \delta\omega_2 t \). Relationships (14) and (15) are derived from Eq. (8) and Eq. (13). One can also make use of the third recorded band \( \tilde{H}_1 \) and the property \( J_{-1}(\phi_0) = -J_1(\phi_0) \) to derive \( z_0 \approx \lambda/(2\pi) \left| \tilde{H}_1/\tilde{H}_0 \right| \).

To perform the measurement, an optical LO consisting of the combination of three frequency components shifted by \( \Delta\omega_1, \Delta\omega_2, \) and \( \Delta\omega_3 \) (Eq. 12) was realized. Those shifts were chosen to yield non-symmetrical (non-opposed) algebraic modulation frequencies \( \delta\omega_1, \delta\omega_2, \) and \( \delta\omega_3 \) in the detector bandwidth in order to avoid spurious aliasing or cross-talk effects. To do so, we made use of phase-locked RF signals generated by frequency-synthesizers at the carrier frequency \( \omega_C, \omega_C + \delta\omega_1, \omega + \delta\omega_2, \) and \( \omega_C + \delta\omega_3 \), where the shifts used to...
generate the three RF bands were \( \delta \omega_1'/(2\pi) = -1.25 \text{ Hz} \),
\( \delta \omega_2'/(2\pi) = 6.25 \text{ Hz} \), \( \delta \omega_3'/(2\pi) = -\gamma_0 \text{ Hz} \) (see Tab. I).
As sketched in Fig. 1 those signals were mixed and
combined to drive a set of acousto-optic modulators
(AA Opto Electronic) designed to operate around
\( \omega_C/(2\pi) = 80 \text{ MHz} \), from which opposite diffraction
orders were selected. The resulting modulation frequencies
of the holograms (Eq. 13) were \( \delta \omega_1 = \delta \omega_1' + \delta \omega_2' \),
\( \delta \omega_2 = \delta \omega_1' - \delta \omega_2' \), \( \delta \omega_3 = \delta \omega_1' - \delta \omega_2' \). The three sideband
components \( H_{-1}, H_0 \), and \( H_1 \), encoded at 5 Hz, -2.5 Hz,
and -7.5 Hz respectively, are visible on the magnitude of
the discrete Fourier spectrum (Eq. 13) reported in Fig. 3.
Spectral maps of the vibration amplitude \( z_0(\omega) \) were
calculated from a set of sequential measurements at each
frequency. We took 3000 sequences of \( N = 8 \) raw interferograms I
sampled at a frame rate of \( 10 \text{ mV} \). The first resonance frequencies of
the lamellophone's cantilevers are observed between
500 Hz and 2500 Hz (Media 1). Plots of the vibration amplitude
of the 1st, 5th, and 17th cantilevers versus excitation frequencies
ranging from 536 Hz to 546 Hz. The values of
\( \delta \omega_1 \) are randomized from the measurement
of one frequency point to the next. Hence the phase
retardation \( \psi(t) \) cannot be retrieved. To prevent reference
phase randomization between measurements, a chirp of the
frequency \( \omega \) was performed. It consisted of a linear
drift with time \( t \) of the excitation frequency from
\( \omega_f/(2\pi) = 536 \text{ Hz} \) to \( \omega_f/(2\pi) = 546 \text{ Hz} \) in \( T = 99.2 \text{ s} \)
\( \omega(t) = \omega_1 + (\omega_f - \omega_1) t/T \) \hspace{1cm} (16)
Two out of the three components of the optical LO

\[
\begin{array}{c|c}
\text{angular frequency} & \text{value} \\
\hline
\delta \omega_1' & -1.25 \text{ Hz} \\
\delta \omega_2' & 6.25 \text{ Hz} \\
\delta \omega_3' & -\gamma_0 \text{ Hz} \\
\delta \omega_1 = \delta \omega_1' + \delta \omega_2' & 5 \text{ Hz} \\
\delta \omega_2 = \delta \omega_1' - \delta \omega_2' & -2.5 \text{ Hz} \\
\delta \omega_3 = \delta \omega_1' - \delta \omega_2' & -7.5 \text{ Hz} \\
\Delta \omega_1 = -\omega - \delta \omega_1 & \\
\Delta \omega_2 = \delta \omega_2 & \\
\Delta \omega_3 = \omega - \delta \omega_3 & \\
\end{array}
\]

**TABLE I:** Frequency shifts used in the experiments.

A finer screening around the resonance of the first cantilever was performed, from 248 sequences of \( N = 8 \) raw interferograms, for excitation frequencies ranging from 536 Hz to 546 Hz. The values of \( z_0(\omega) \), spatially averaged over the extent of the resonant cantilever, arrowed in Fig. 2(b), are marked as points in the plot reported in Fig. 3(a). But \( \psi(t) \) is randomized from the measurement of one frequency point to the next. Hence the phase retardation \( \psi \) cannot be retrieved. To prevent reference phase randomization between measurements, a chirp of the frequency \( \omega \) was performed. It consisted of a linear
drift with time \( t \) of the excitation frequency from
\( \omega_f/(2\pi) = 536 \text{ Hz} \) to \( \omega_f/(2\pi) = 546 \text{ Hz} \) in \( T = 99.2 \text{ s} \)
\( \omega(t) = \omega_1 + (\omega_f - \omega_1) t/T \) \hspace{1cm} (16)
Two out of the three components of the optical LO

\[
\begin{array}{c|c}
\text{angular frequency} & \text{value} \\
\hline
\delta \omega_1' & -1.25 \text{ Hz} \\
\delta \omega_2' & 6.25 \text{ Hz} \\
\delta \omega_3' & -\gamma_0 \text{ Hz} \\
\delta \omega_1 = \delta \omega_1' + \delta \omega_2' & 5 \text{ Hz} \\
\delta \omega_2 = \delta \omega_1' - \delta \omega_2' & -2.5 \text{ Hz} \\
\delta \omega_3 = \delta \omega_1' - \delta \omega_2' & -7.5 \text{ Hz} \\
\Delta \omega_1 = -\omega - \delta \omega_1 & \\
\Delta \omega_2 = \delta \omega_2 & \\
\Delta \omega_3 = \omega - \delta \omega_3 & \\
\end{array}
\]

**TABLE I:** Frequency shifts used in the experiments.

(\( \text{Eq. 16} \)) were chirped as well via \( \omega(t) \) throughout the
acquisition. During the time lapse \( T \), a sequence of
248 \times 8 = 1984 \) raw interferograms I was steadily
recorded. In that manner, \( \psi(t) \) remained constant.
Amplitude \( z_0(\omega) \) and phase \( \psi(\omega) \) maps at each frequency \( \omega \)
were calculated from the demodulation of \( N = 8 \) con-
ssecutive raw frames, reported in media 2. The complex
values of these maps were averaged over the spatial
extent of the first cantilever and reported in Fig. 3 (blue
lines). In agreement with Eq. 4 for non-zero viscosity,
a phase shift of \( \sim \pi \) is observed at the resonance frequency
\( \omega_r \sim 541.3 \text{ Hz} \). The theoretical resonance lines
in Fig. 4 were determined for a resonance frequency of
the undamped oscillator \( \omega_0/(2\pi) = 541.3 \text{ Hz} \) and a
dimensionless damping ratio \( \zeta = 2 \times 10^{-5} \), for which
Eq. 3 and Eq. 4 best fit the experimentally-measured
vibration amplitude.

In conclusion, we performed optical path length modu-
lization imaging by time-averaged heterodyne holography
in off-axis and frequency-shifting conditions. To do
so, modulation sidebands were acquired simultaneously
through coherent frequency-division multiplexing. Additionally, a linear chirp of the excitation and the detection frequencies allowed to map the local mechanical phase retardation of a resonant cantilever with respect to the excitation signal without stroboscopy. The proposed method enabled robust and quantitative narrowband imaging of out-of-plane vibration amplitude and phase.

We gratefully acknowledge support from Fondation Pierre-Gilles de Gennes (FPGG014), Agence Nationale de la Recherche (ANR-09-JCJC-0113, ANR-11-EMMA-046), région Île-de-France (C’Nano, AIMA), and the “investments for the future” program (LabEx WIFI: ANR-10-LABX-24, ANR-10-IDEX-0001-02 PSL*).

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