Spectrum sensing in single channel and multi-channel cognitive radio networks

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ABSTRACT
Sensing the existence or absence of primary user is the major chore of cognitive radio networks. Nevertheless, Spectrum sensing is the core process of cognitive radio and with target to find idle channels. Various detection techniques exist, however, energy detection is considered as the most used detector because of its lower computational cost. In this paper, we proposed a study of throughput for a cognitive radio system. We had two scenarios, in the first scenario; a study of throughput against probability of false alarm was done; where, only one channel is sensed, to maximize the individual channel throughput. In the second scenario, multi-channel is sensed to maximize the overall system capacity. In addition, different number of channels is considered with different sensing times and at different throughput costs. The performance of the network has been investigated in terms of maximum throughput for optimal number of cognitive radio channels.

Keywords: Cognitive radio
Spectrum sensing
Throughput

1. INTRODUCTION
Cognitive Radio (CR) has been recently proposed as a smart and agile technology which allows illegal users to utilize the licensed bands [1-5]. CR system has two users, Primary User (PU) and Secondary User (SU) [6]. Spectrum management is the main function in CR, it has many process like Spectrum Sensing (SS), spectrum decision and spectrum handoff. SS is one of the major functionality distinguishing CR sensors network from traditional Wireless Sensor Networks (WSNs). Spectrum decision where CR network needs to analyze the sensing data and make decision about the channel and transmission parameters. Spectrum handoff when a primary user arrives again to use a previously available channel, CR node must detect this activity and handoff to another sensed channel within a certain time [7]. To ensure that the operations of the primary users are not affected, it must possess the spectrum-sensing capability. Meaning that, the ability of detecting the presence of primary signals in the bands of interest. Spectrum sensing has many techniques (e.g. Matched filter, energy detection, feature detection, interference temperature) [8]. In this paper, energy detection is used, because it is a common technique for spectrum sensing which is simple and fast, works better in high Signal to Noise Ratio (SNR), but it is not robust at low SNR and cannot differentiate between noise and signal [9]. The CR system may be one channel or Multi-channels, each system has advantages and disadvantages, its use depend on what we need. In CR, the secondary users need to speculatively sense the idle channels [10-13]. Once an idle channel is sensed, the secondary system will access this channel. Therefore, spectrum sensing, [14-17] as an essential problem in CR, requests the secondary users to efficiently and effectively detect the presence of the primary signals. There are two measures that related to the sensing performance. First one is the probability of detection, which is the probability of the existence of...
the primary user being detected. Another is the probability of false alarm, which is the probability that the primary user is detected as existence, but actually it is absent [18-25].

Main design principles, potential, advantages, application areas and network architectures of CRSNs are introduced in [1]. In [3] the optimal sensing has been proposed to maximize the channel throughput. The proposed optimal Cooperative Spectrum Sensing (CSS) settings for both the single channel sensing and wide-band sensing are analyzed and calculated in detail by using some simple but reliable methods. In [4] an optimal multiband joint detection method is proposed to increase the performance of secondary user over multiple frequency bands. In [5] the researchers studied the problem of designing the sensing slot duration to maximize the achievable throughput for the secondary users under the constraint that the primary users are sufficiently protected. Using energy detection. In [6] multiband joint detection has proposed for wideband spectrum sensing in CR networks. The basic strategy is to take into account the detection of primary users jointly across a bank of narrowband sub bands rather than considering only one single band at a time.

Authors in [8] investigated the performance of spectrum sensing for Wi-Fi network where customer-premises equipment is using CR technology. It is found that the throughput becomes maximum at optimal sensing time. Maximum throughput of the network has been investigated for different number of optimal CR users and maximum throughput decreases as the number of optimal CR users increases. In [13] the change of the average effective capacity has been studied in a single frame with the number of channels under different PU traffic rates. It provides a reference for the establishment of cognitive radio system under the different licensed networks. Authors in [14] presented an optimal multiband sensing-time-adaptive joint detection (MSJD) framework for wideband spectrum sensing. In [20] authors introduced an Orthogonal Frequency Division Multiplexing (OFDM) based cognitive multi relay network is investigated to maximize the transmission rate of the cognitive radio (CR) with enhanced fairness among CR users with interference to the primary users (PUs) being managed below a certain threshold level.

In this paper, we are going to study single and multi-channel throughput, make discussion at both of them and search how to find optimal number of channels in multi-channel system. The rest of this paper is organized as following. Section 2 presents energy detection, single channel and multi-channel , Section 3 discusses simulation results, and finally the paper is concluded in Section 4.

2. RESEARCH METHOD

A single and multi-channel are two system models, the first one has single channel with primary users (PUs) and secondary users (SUs), the second one has multi-channels, we study the behave of each system to see how the SU can access the channel without interfering the PU.

The Energy Detection (ED) doesn’t need any information about the primary user’s signal. It compares the received signal power to the noise power, if the signal power is greater than the pre-assumed noise power level, then the detector decide that the primary signal presence. Without loss of generality, we assume that the noise power is identical at different secondary users. The detection problem can be summarized using two binary hypotheses that can be addressed as $H_0$ and $H_1$ denote the absence and the presence of the primary user, respectively. Therefore the two hypotheses can be formulated as in [7].

$$H_0 : X(n) = V(n)$$

$$H_1 : X(n) = S(n) + V(n) \quad (1)$$

Where $X(n)$ is the received signal at cognitive radio node, $S(n)$ is the transmitted primary user signal, and $V(n)$ is the noise with variance $\sigma^2$.

In single channel, secondary users access to the primary channel only when the channel is sensed to be idle. Let $\delta$ denote the probability that the channel is idle [1]. Therefore, the probability that the channel occupied by only the primary users is $\delta Q_0$ , the probability that the channel occupied simultaneously by both primary users and secondary users is $\delta (1 - Q_d)$ and the probability that the channel is occupied only by the secondary users is $(1 - \delta) \delta$. Let $T_p$ and $T_p'$ denote the throughput of the primary system without and with the existence of the secondary user, respectively. Let $T_s$ and $T_s'$ denote the throughput of the secondary system without and with the existence of primary user, respectively [1]. Therefore the channel throughput $J$ can be formulated as in [1].

$$J = \delta T_p Q_d + \delta (T_p' + T_s') (1 - Q_d) + (1 - \delta) (1 - Q_s) T_s \quad (3)$$

We can rewrite $(3)$ as
\[ J = a_0 + a_1 Q_1 - a_2 Q_f \]  
(4)

Where the final false-alarm probability \( Q_f \) and the final detection probability \( Q_d \). Note that, \( a_0, a_1 \) and \( a_2 \) are constants in the optimization problem \([1]\).

In multi-channel, the performance of spectrum sensing has been investigated in terms of optimal number of CR users \((n_{opt})\) in cooperation \([8]\)(as every SU represent one channel in our system), throughput \((R(n_{opt}, t))\) for sensing time and maximum throughput \(R_{Max}(n_{opt})\) for optimal number of CR users. The received signal at each CR is sampled at sampling frequency \( f_s \). Each frame of CR consists of spectrum sensing time \((\tau)\) and data transmission time \((T - \tau)\), where \( T \) is the total frame time. Let \( K \) be the number of samples available during \( \tau \). Hence the number of samples, \( K = t \cdot f_s \) \([14, 8]\).

\[ P_f(t) = \frac{1}{2} \operatorname{erfc}\left(\frac{1}{\sqrt{2}} \left(\frac{\lambda}{\sigma^2} - 1\right) \sqrt{R}\right) \]  
(5)

\[ P_d(t) = \frac{1}{2} \operatorname{erfc}\left(\frac{1}{\sqrt{2}} \left(\frac{Y - 1}{\sigma^2} - \frac{k}{\sqrt{2}Y + 1}\right)\right) \]  
(6)

Where \( \gamma \) is the SNR at the CR receiver and \( \lambda \) is the decision threshold. To ensure reliable sensing performance, detection probability must be high. The decision threshold as in \([8]\),

\[ \lambda = \sigma^2 \left[\sqrt{2}(2Y + 1) \operatorname{erfcinv}(2PD) + \sqrt{Y}\right] + 1 \]  
(7)

A CR user can transmit data when the PU is not active. Hence, the CRs can transmit data when the decision goes in favor of false alarm or missed detection. Let us consider not that denotes the number of CRs in spectrum sensing. The throughput for the overall false alarm probability is \([8, 5]\)

\[ R_0 = \frac{T - \tau}{T} C_0 \left(1 - Q_{f_{opt}}(t)\right) P(H_0) \]  
(8)

Where \( C_0 \) is the throughput in the absence of PU.

The throughput for the overall missed detection probability is

\[ R_1 = \frac{T - \tau}{T} C_1 \left(1 - Q_{d_{opt}}(t)\right) P(H_1) \]  
(9)

Where \( C_1 \) is the throughput in the presence of PU.

From (5),(6) we get

\[ Q_{f_{opt}} = 1 - (1 - P_f(t))^2 \]  
(10)

\[ Q_{d_{opt}} = 1 - (1 - P_d(t))^2 \]  
(11)

From the above discussion we can get total throughput \( R(n_{opt}, t) \) is a function of \( n_{opt} \) and \( t \). Hence \( R(n_{opt}, t) \) of the CR network can be written as

\[ R(n_{opt}, t) = \frac{T - \tau}{T} \left[ C_0 \left(1 - Q_{f_{opt}}(t)\right) P(H_0) + C_1 \left(1 - Q_{d_{opt}}(t)\right) P(H_1)\right] \]  
(12)

For fixed \( n_{opt} \), \( R(n_{opt}, t) \) is concave means there is a maxima of \( R(n_{opt}, t) \) i.e., \( R_{Max}(n_{opt})\)

When \( t = t_{opt} \), the \( R(n_{opt}, t) \) reaches at \( R_{Max}(n_{opt}) \).

We can say that \( C \) is indicates the capacity (we can say that, it is cost spend to get high throughput) gained if the primary user in sub-band is absence. Formulated as in \([19]\),

\[ C = B \sum_{i=1}^{n} \log_2 \left(1 + \frac{E_b h_i}{N_0}\right) \]  
(13)

Where, \( E_b \) represents the energy of each bit of information, \( h_i \) represents the fading coefficient of the secondary user, \( N_0 \) represents noise density.
3. RESULTS AND ANALYSIS

In this section, we provide analytical and simulation results to investigate the performance of spectrum sensing with energy detection method in the considered scenarios.

3.1. Single Channel

Figure 1 shows result of channel throughput $J$ versus $P_f$ at $\lambda = 0.2$ in which sensing parameters are given as average $SNR = 8dB$, time bandwidth product $N = 10$, number of secondary users $M = 4$, and the system parameters $a_0 = 12, a_1 = 7, a_2 = 9$ [3]. For a given $\lambda$, it is clear that when $P_f$ reaches 0.2 throughput starts to decrease slowly till $P_f$ reaches 0.4, throughput begins to decrease with higher rate.

![Figure 1. Throughput vs probability of false alarm](image1)

3.2. Multi-Channel

It is considered that the primary user is using BPSK modulation to transmit its data with 3 MHz bandwidth. The maximum time for which the secondary network unaware of the primary activity is chosen such that $f_sT=3000$ [4]. The frame time of detection cycle is 100ms and target detection probability is 0.7. We choose $P(H_0) = 0.8, P(H_1) = 0.2, C_0 = 6.6582$ and $C_1 = 6.6137$.

Figure 2 by comparison with [13] we obtained that at $t = 3ms, P_f$ in reference system reaches to 0.5 but in our proposed system that we improved, $P_f$ reduces to 0.15. This means that improvement of the system is by 30%.

Figure 3 shows the throughput as a function of sensing time for $SNR = 10dB, P_d = 0.7$. In this case at $n=15$, it is found that as the sensing time increased, the throughput increased until $t = 2ms$, after that throughput is stopped increasing with increasing time.

![Figure 2. Sensing time vs probability of false alarm](image2)

![Figure 3. Throughput vs sensing time](image3)

Figure 4 shows throughput for network at optimal number of CRs has been compared when $n = [1, 5, 10, 15]$. We obtained that as the probability of false alarm increases, the throughput of CR network decreases. Hence there is an optimal sensing time in each case for which the throughput is maximum. When
$P_f=0.15$ and $n=5$, the throughput $R=2.3$. At $n=10$ and the throughput $R=1$, which means that when $n$ is doubled, the throughput decreased by 43%. By comparing throughput at $P_f=0.2$ when $n=1$, we obtain that throughput is higher in single channel than in multi-channel, it is a logical case.

Figure 5 shows the throughput as a function of time with different costs, working at $n=15$. We obtain that when we increase the cost the peak value of throughput is increased. When $t=2\text{ms}$, at $C=9.9672$ and the throughput $R=7.9$, at $C=6.6582$ and the throughput $R=5$. This means improving throughput by 63% with spending added cost 66%.

Figure 6 shows the effect of varying cost at different number of CRs, working at $t=0.2\text{ms}$. We obtain varying throughput as $n$ (number of CRs) increases throughput decreases. When $n=5$, at $C=9.9672$ and the throughput $R=3.1$, at $C=6.6582$ and the throughput $R=2.2$. This means improving throughput by 71% with spending added cost by 65%.

**4. CONCLUSION**

The optimal sensing settings to maximize the channel throughput, which is one of great practical interest than other sensing objectives, have been proposed in our work. The proposed optimal settings for both the single channel sensing and wide-band sensing is analyzed and calculated in detail by using some simple but reliable methods. We compared between single channel and multi-channel in throughput to get maximum throughput in both systems. It is an improved system because our target in cognitive radio to have minimum probability of false alarm, our proposed system decreased the probability of false alarm by 30%. From result, when we increase the cost we increase throughput by 63% to 71% depending on number of CRs. Theoretical analysis and simulation results have been shown that the proposed optimal settings can substantially improve the channel throughput in cognitive radio networks.

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