Model-independent constraints on dark energy and modified gravity with the SKA

Gong-Bo Zhao 1, 2, David Bacon 2, Roy Maartens 3, 2, Mario Santos 3, 4, Alvise Raccanelli 5, 6, 7

1 National Astronomy Observatories, Chinese Academy of Science, Beijing, 100012, People’s Republic of China
2 Institute of Cosmology and Gravitation, University of Portsmouth, Portsmouth, PO1 3FX, United Kingdom
3 Department of Physics, University of the Western Cape, Cape Town 7535, South Africa
4 SKA SA, 4th Floor, The Park, Park Road, Pinelands, 7405, South Africa
5 Department of Physics & Astronomy, Johns Hopkins University, 3400 N. Charles St., Baltimore, MD 21218, USA
6 Jet Propulsion Laboratory, California Institute of Technology, Pasadena CA 91109, USA
7 California Institute of Technology, Pasadena CA 91125, USA

Employing a nonparametric approach of the principal component analysis (PCA), we forecast the future constraint on the equation of state $w(z)$ of dark energy, and on the effective Newton constant $\mu(k,z)$, which parameterise the effect of modified gravity, using the planned SKA HI galaxy survey. Combining with the simulated data of Planck and Dark Energy Survey (DES), we find that SKA Phase 1 (SKA1) and SKA Phase 2 (SKA2) can well constrain 3 and 5 eigenmodes of $w(z)$ respectively. The errors of the best measured modes can be reduced to 0.04 and 0.023 for SKA1 and SKA2 respectively, making it possible to probe dark energy dynamics. On the other hand, SKA1 and SKA2 can constrain 7 and 20 eigenmodes of $\mu(k,z)$ respectively within 10% sensitivity level. Furthermore, 2 and 7 modes can be constrained within sub percent level using SKA1 and SKA2 respectively. This is a significant improvement compared to the combined datasets without SKA.
1. Introduction

The physical origin of the acceleration of the universe remains unknown since its discovery in 1998 using supernovae (SN) observations (Riess et al. 1998; Perlmutter et al. 1999). It might imply that there exists a repulsive ‘dark energy’ component dominating the universe, or that we need a better understanding of the law of gravity, i.e., the general relativity (GR) might need to be modified on cosmological scales (For a recent review of modified gravity theories, see Clifton et al. 2012). Although dark energy (DE) and modified gravity (MG) can accelerate the universe at the background level in the same way after the required tuning, the degeneracy can be broken when the cosmic structure formation is investigated.

In this era of precision cosmology, a combination of multiple observation probes including SN, cosmic microwave background (CMB), and large scale structure (LSS) surveys is key to unveil the mystery of the cosmic acceleration (Weinberg et al. 2013). This is because different kinds of surveys can be highly complementary, e.g., the weak lensing (WL) and redshift surveys are able to probe $\gamma(k,z)$, quantifying the deviation of photon’s trajectory from the geodesics, and $\mu(k,z)$, the time and spatial variation of the Newton’s constant respectively, which are two different effects predicted by a wide range of MG models, making the combination of WL with redshift surveys robust for GR tests, as well as for the dark energy studies.

Given that the CMB and WL surveys of Planck (Planck Collaboration et al. 2014) and Dark Energy Survey (DES) ¹ are accumulating data, we need large redshift surveys to complement. The BOSS spectroscopic survey (Anderson et al. 2014) of SDSS-III is currently the largest redshift survey worldwide, mapping the 10,000 square degree sky up to $z = 0.7$ by tracing 1.5 million luminous galaxies. It will be succeeded by eBOSS ², a multi-tracer spectroscopic survey of SDSS-IV, which will focus on a smaller patch of the sky (7500 square degree) but going deeper. According to the forecast, it will achieve 1-2% distance measurement from the baryon acoustic oscillations (BAO) between $0.6 < \ z < 2.5$. The Square Kilometre Array (SKA) ³ HI galaxy redshift survey can provide us with accurate redshifts (using the 21cm line) of millions of sources over a wide range of redshifts, making it an ideal redshift survey for cosmological studies (Bull et al. 2015; Raccanelli et al. 2015; Bacon et al. 2015; Kitching et al. 2015; Santos et al. 2015; Abdalla et al. 2015).

Traditionally, observational constraints on DE or MG using either current or future data are usually performed in a parameterised fashion, i.e., the equation of state of DE, $w(z)$, or the $\mu(k,z)$ and $\gamma(k,z)$ functions quantifying the effect of MG (Zhao et al. 2009b) ⁴, are parameterised using assumed function forms, and then the observational constraints on these parameters are worked out. Simple as it is, this approach has its drawbacks,

- It may cause theoretical bias: the result largely depends on the functional form used for the parametrisation, which is a priori. The functional forms are usually chosen for the purpose of simplicity, or for the assumed theoretical consistency, or for both;

---

¹More details of the Dark Energy Survey are available at http://www.dark-energysurvey.org/
²More details of the eBOSS survey are available at http://www.sdss.org/sdss-surveys/eboss/
³More details of the SKA survey are available at https://www.skatelescope.org/
⁴There are other ways to parameterise the effect of MG, e.g., see Baker et al. (2013).
The number of parameters are usually minimised, e.g., the CPL parametrisation (Chevallier & Polarski 2001; Linder 2003) of $w(z)$ has 2 parameters, while the BZ parametrisation (Bertschinger & Zukin 2008) for MG has 5 parameters. This can yield a reasonably good constraint on the reconstructed $w(z)$, or the MG functions even when data is weak, but it might under fit the data when data is excellent.

However, in nonparametric methods, including the principal component analysis (PCA), it is the assumption, rather than the number of parameters, that is minimised, hence it can largely avoid the theoretical bias.

In this chapter, we use the PCA method to perform the forecast of $w(z)$ and $\mu(k, z)$ using a SKA HI redshift galaxy survey.

2. Methodology

In this section, we employ a standard Fisher matrix technology (Tegmark et al. 1997) to perform the future forecast.

2.1 The Fisher matrix formulism

For a redshift survey, the Fisher matrix formalism reads (Seo & Eisenstein 2007)\(^5\),

$$F_{ij} = \int_{-1}^{1} d\mu \int_{k_{\mathrm{min}}}^{k_{\mathrm{max}}} dk \frac{\partial \ln \tilde{P}(k, \mu)}{\partial p_i} \frac{\partial \ln \tilde{P}(k, \mu)}{\partial p_j} V_{\mathrm{eff}}(k, \mu) \frac{k^2}{8\pi^2}$$

(2.1)

$$\tilde{P}(k, \mu) = (b + f \mu^2)^2 P(k) e^{-k^2 \mu^2 \Sigma^2}$$

(2.2)

$$V_{\mathrm{eff}}(k, \mu) = \left[ \frac{n P(k)(1 + \beta \mu^2)^2}{n P(k)(1 + \beta \mu^2)^2 + 1} \right]^2 V_{\mathrm{sur}}$$

(2.3)

where $\tilde{P}(k, \mu), V_{\mathrm{eff}}$ denote the power spectrum in redshift space and the effective volume respectively, and $V_{\mathrm{sur}}$ is the actual volume of the redshift survey. We have used the Kaiser formula, i.e., Eq (2.2) to evaluate $\tilde{P}(k, \mu)$, where $P(k)$ is the linear matter spectrum calculated using CAMB (Lewis et al. 2000), $b$ and $f$ are the linear bias and the growth function respectively. To account for the Finger of God (FoG) effect, we have chosen $\Sigma$ to be 4 Mpc, which is consistent with simulations.

The Fisher matrix formulae for CMB and WL surveys are elaborated in Zhao et al. (2009b).

2.2 Specifications of future SKA HI surveys

A future SKA HI redshift survey will trace the galaxies at radio wavelengths, and the redshifts will be measured precisely using the emission lines. In this work, we consider Phase 1 and Phase 2 of SKA HI surveys (dubbed SKA1 and SKA2 respectively). SKA1 will achieve an RMS flux sensitivity of $S_{\mathrm{rms}} \simeq 70 - 100 \mu Jy$ with SKA1-MID or SUR, surveying over 5000 deg\(^2\) in 10,000 hours. The expected total number of galaxies in Phase 1 is roughly 5 million at redshift $z \lesssim 0.5$ with a 5$\sigma$ detection. In Phase 2, a 10,000 hours survey over 30,000 deg\(^2\) will detect one billion galaxies.

\(^5\)Note that this is the Fisher matrix for a given redshift bin. The final Fisher matrix is the sum over the Fisher matrices of individual redshift bins.
at a 10σ detection level. The expected galaxy distribution and bias for SKA1 (SKA2) is shown in Fig 1. For more details of the survey specifications, see Santos et al. (2015). Although SKA1 is not able to compete with the BOSS survey, SKA2 will surpass any planned spectroscopic surveys in the optical bands at $z \lesssim 1.4$.

2.3 Cosmological parameters

To be generic, we parameterise the universe using parameters

$$P = \{\Omega_b h^2, \Omega_c h^2, h, \tau, n_s, A_s, w_i, \mu_{ij}, \gamma_{ij}\}$$

(2.4)

where $\Omega_b h^2$ and $\Omega_c h^2$ are energy density of baryons and cold dark matter respectively, $h$ is the Hubble constant, $\tau$ is the optical depth, $n_s$ and $A_s$ are the spectral index and the amplitude of the primordial power spectrum respectively. $w$ denotes the equation-of-state of dark energy. In general, we treat $w(z)$ as a unknown function and determine how many degrees of freedom of it can be constrained using the PCA method (Huterer & Starkman 2003; Crittenden et al. 2009, 2012; Zhao et al. 2009a; Asaba et al. 2013; Hall et al. 2013). To do this, we bin $w$ in the late-time universe, namely, $0 \leq z \leq 30$ using $M + 1$ $z$-bins, and consider the value of $w$ in each bin as an independent parameter. Since the surveys we consider in this work will not be able to probe $z > 3$ in detail, we use $M$ bins linear in $z$ for $0 \leq z \leq 3$ and a single bin for $3 \leq z \leq 30$.

The $\mu$ and $\gamma$’s are modified gravity parameters and they are defined as follows.

In Newtonian gauge, the linear scalar perturbations to the flat Friedmann-Robertson-Walker metric read,

$$ds^2 = -a^2(\eta)[(1 + 2\Psi(\vec{x}, \eta))d\eta^2 - (1 - 2\Phi(\vec{x}, \eta))d\vec{x}^2],$$

(2.5)

where $\eta$ is the conformal time and $a(\eta)$ the scale factor. In Fourier space, one can write (Hu & Sawicki 2007; Bertschinger & Zukin 2008),

$$k^2\Psi = -\mu(k, a)4\pi G a^2 \rho \Delta$$

(2.6)

$$\Phi/\Psi = \gamma(k, a)$$

(2.7)

where $\Delta$ is the comoving matter density perturbation. The function $\gamma$ describes anisotropic stresses, while $\mu$ describes a time- and scale-dependent rescaling of Newton’s constant $G$, as well as the effects of DE clustering or massive neutrinos. In $\Lambda$CDM, the anisotropic stress due to radiation is negligible during matter domination, thus $\mu = \gamma = 1$.

Similar to $w(z)$, we treat $\mu(k, a)$ and $\gamma(k, a)$ as unknown functions and forecast how well we can constrain the eigenmodes of them using PCA. Since they are 2-variable functions in both $k$ and $a$, we have to pixelise them in the $(k, z)$ plane. We pixelise the late-time and large-scale universe ($0 \leq z \leq 30, 10^{-5} \leq k \leq 0.2 \ h\text{Mpc}^{-1}$) into $M + 1$ $z$-bins and $N$ $k$-bins, with each of the $(M + 1) \times N$ pixels having independent values of $\mu_{ij}$ and $\gamma_{ij}$. We consider $w(z)$ as another unknown function, allowing each of the $M + 1$ $z$-bins to have an independent value of $w_i$. We use $M$ bins linear in $z$ for $0 \leq z \leq 3$ and a single bin for $3 \leq z \leq 30$. We choose $M = N = 20$ and have checked that this pixelisation is fine enough to ensure the convergence of the results. We use logarithmic $k$-bins on superhorizon scales and linear $k$-bins on subhorizon scales, to optimize computational efficiency. As in Zhao et al. (2009b), we only consider information from scales well-described by linear perturbation theory, which is only a fraction of the $(k, z)$-volume probed by future surveys. Since the
evolution equations (Zhao et al. 2009b) contain time-derivatives of $\mu(k,z)$, $\gamma(k,z)$ and $w(z)$, we follow Crittenden et al. (2009) and Zhao et al. (2009a) and use hyperbolic tangent functions to represent steps in these functions in the $z$-direction, while steps in the $k$-direction are left as step functions. The total number of free parameters in our forecast is therefore $(M+1)(2N+1) + 17 = 878.$

2.4 The principal component analysis (PCA) method

The PCA method is a traditional method in data analysis. It helps to identify the principal components (PCs) of data by maximising the data covariance matrix. In cosmology, PCA has been used in determining the well-constrained combinations of cosmological parameters, e.g., the binned equation of state $w(z)$ of dark energy (Huterer & Starkman 2003; Crittenden et al. 2009, 2012) and the pixelised 2-variable functions of $\mu(k,z)$ and $\gamma(k,z)$ (Zhao et al. 2009a; Asaba et al. 2013; Hall et al. 2013), which quantify the deviation from general relativity on cosmological scales.

Generically, the PCA method can be formulated as follows. Let $F$ be an $N \times N$ Fisher information matrix for a parameter set $P = \{p_1, p_2, ..., p_N\}$. We can find the eigenmodes of $F$ by matrix diagonalisation, namely,

$$F = W^T \Lambda W,$$

where $\Lambda = \text{diag}(\lambda_1, \lambda_2, ..., \lambda_N)$, and $W$ is the transformation matrix relating $P$ to $Q$, which is a set

\[\text{Figure 1: Upper panel: The expected galaxy distribution for SKA1 and SKA2; Lower panel: the corresponding bias as a function of redshift.}\]
of new parameters $Q = \{q_1, q_2, \ldots, q_N\}$. $P$ and $Q$ are related via,

$$Q = WP$$  \hspace{1cm} (2.9)

The matrices $\Lambda$ and $W$ store the eigen-values and eigen-vectors of $F$: $W$ tells how to map the old correlated parameters, the $p$’s, to the new orthogonal ones, the $q$’s, and $\Lambda$ quantifies the uncertainty on the $q$’s. The best measured parameter is the $q$ with the minimal error (the one corresponding to the maximum entry in matrix $\Lambda$).

For dark energy, the $p$’s are the binned $w(z)$ in redshift $z$. $W$ helps to locate the ‘sweet-spots’ (the redshifts where the error on $w(z)$ get minimised), and $\Lambda$ quantifies how ‘sweet’ they are (the size of errors when measuring these modes). For modified gravity, the $p$’s are the pixelised functions of $\mu(k,z)$ and $\gamma(k,z)$ in the $(k,z)$ plane, and the eigen-vectors in this case are 2D surfaces.

3. Results

For a given set of parameter values, we use MGCAMB (Zhao et al. 2009b; Hojjati et al. 2011) to compute the observables. We generate numerical derivatives of observables with respect to parameters, and use the specifications for the experiments to compute the Fisher information matrix, which defines the sensitivity of the experiments to these parameters (see Zhao et al. 2009b for computational details). Our fiducial values are in all cases $\Lambda CDM$: $\gamma_{ij} = \mu_{ij} = -w_i = 1$ for all $i$ and $j$, and the fiducial values of the other parameters are those of Planck.

Besides the SKA HI surveys, we consider the two-point correlations (both auto- and cross-) between weak lensing shear (WL), and cosmic microwave background (CMB) temperature anisotropy, plus the CMB E-mode polarization and its correlation with the CMB temperature. Detailed descriptions of our assumptions for each measurement are found in Zhao et al. (2009b). WL is sourced by the sum of the potentials $(\Psi + \Phi)$. CMB data probe the Integrated Sachs-Wolfe effect (ISW) which depends on $\partial (\Phi + \Psi)/\partial \eta$. Thus, measuring WL over multiple redshift bins, along with CMB data, yields information about the relation between $\Psi$ and $\Phi$ and their response to matter density fluctuations. For our forecasts, we assume the following probes: Planck (Planck Collaboration et al. 2014) for CMB, and DES for WL.

In what follows in the section, we shall present the results of our forecast for dark energy and modified gravity respectively.

3.1 Dark Energy constraints

In this section, we focus on DE constraints in the framework of general relativity. Therefore we fix the $\mu$ and $\gamma$ pixels to be unity, but vary the remaining parameters in Eq (2.4) simultaneously. After marginalising over other parameters, we perform a PCA on the $w$ bins.

The result is shown in Figs 2 and 3. In Fig 2, we show the 68% CL forecasted error on the part of the principal components (PCs) for four different data combinations. As shown, within the level of $\sigma(\alpha_i) < 0.5$, Planck alone can only constrain 1 mode (the distance to the last scattering surface); Planck + DES can constrain 2 modes, while adding in SKA1 or SKA2 can constrain 3 and 5 eigenmodes to this level. In particular, the best measured modes using SKA1 and SKA2 (combined with Planck and DES) can be determined at the level of $\sigma(\alpha_1) = 0.04$ and $\sigma(\alpha_1) =$
0.023 respectively. This is a significant improvement given that $\sigma(\alpha_1) = 0.25$ (Planck alone) and $\sigma(\alpha_1) = 0.13$ (Planck + DES).

The eigenvectors for the best constrained modes are shown in Fig 3. Roughly speaking, the $n$th best measured mode has $n-1$ nodes, corresponding to the $(n-1)$th time derivative of $w$. Having SKA helps determining the higher derivatives of $w(z)$, which is key to probe dark energy dynamics.

Figure 2: The forecasted 68% CL measurement error on $\alpha_i$, the coefficient of the $i$th principal components of $w(z) + 1$, namely, $w(z) + 1 = \sum_i \alpha_i \epsilon_i(z)$, using different data combinations illustrated in the legend. A weak prior of $\sigma(w(z)) < 1$ was assumed.

3.2 Modified Gravity constraint

Here we consider the most general case, in which we drop the assumption of general relativity. Therefore we vary all the parameters in Eq (2.4) simultaneously and focus on the constraint on the $\mu$ and $\gamma$.

Let us study the expected errors on $\mu(k,z)$\(^7\). The error on any $\mu_{ij}$ is large, and the pixels have highly correlated errors. We take only the $\mu_{ij}$ block of the covariance matrix, thus marginalizing over all other parameters, including the $w_l$ and $\gamma_{ij}$. We invert this block to obtain the Fisher matrix for our $\mu$ values, $F(\mu)$, and diagonalize $F(\mu)$ by writing $F(\mu) = W^T \Lambda W$. We expect, from existing data, that variations in $\mu$ larger than $O(1)$ are unlikely. We enforce this by applying a prior $\lambda_m > 1$ to the matrix $F(\mu)$. This procedure does not affect the well-measured modes, but gives a reference point with respect to which we define poorly constrained modes. Since we compute the full covariance matrix, then marginalize over all but the parameter(s) of interest, our procedure yields the results that we would get for $\mu$ if we simultaneously measured $w$, $\gamma$, and $\mu$. This analysis can be repeated for $\gamma$ or $w$.

\(^7\)We don’t show the $\gamma$ constraint here since redshift surveys don’t constrain $\gamma$ directly.
Figure 3: The best determined eigenvectors (with errors less than 0.5) of \( w(z) \) for different data combinations shown in the legends. The modes are shown, in the order from better constrained to worse, as black solid, red dashed, blue dash-dot, purple dash-dot-dot and brown short dash-dot curves. The short dashed green horizon line shows \( e_i(z) = 0 \).

Measurements of WL and CMB probe combinations of \( \Phi \) and \( \Psi \), so the effects of \( \gamma \), which affects only \( \Phi \), are mixed with those of \( \mu \), which affects both potentials. This yields degeneracy between \( \mu \) and \( \gamma \). But this degeneracy can be broken when SKA is combined since it only measures \( \Psi \) through the RSD.

From Fig. 4, we see that Planck + DES could not constrain any modes within 10% level, but adding in SKA1 can easily help to constrain 7 modes to this level. SKA2 can further increase this number to 20. In particular 2 and 7 modes can be constrained within sub percent level using SKA1 and SKA2 respectively.

Fig. 5 shows three best constrained eigenmodes for \( \mu \) for different data combinations. A first observation is that the modes with more nodes (a node appears when eigensurfaces cross zero) are less constrained. This is intuitive: noisy modes are worse constrained than the smooth modes. The best modes are mainly functions of \( k \) and not \( z \). This is partly because the total observable volume
PCA of dark energy and modified gravity parameters

Gong-Bo Zhao

Figure 4: The forecasted 68% CL error on the coefficients of the principal components of \( \mu(k, z) \) for different data combinations shown in the legend.

in the radial (\( z \)) direction is limited by the dimming of distant objects and, ultimately, the fact that structures only exist at relatively low \( z \). Also, it is related to us considering only linear perturbations in our analysis, since at small \( z \) the observable volume is too small to fit the small \( k \)-modes that are still in the linear regime. Hence, there is more volume available for studying the spatial distribution of structure than the radial distribution.

For Planck+DES, we see a clear degeneracy in the \( k \) and \( z \) dependences of the modes. This is because changing \( \mu \) at some point \((k, z)\) should have the same impact on the observables as a change at a larger scale but later time. Interestingly, this \( k \) and \( z \) dependence goes away when SKA is combined. This is simply because SKA constrains \( \mu \) very well via the RSD effect, which means that data can well distinguish the effect between the variation of \( \mu \) in \( k \) and in \( z \).

4. Conclusion and Discussions

In this work we apply the PCA method to investigate the constraint on dark energy and modified gravity using the future SKA HI redshift surveys, combined with CMB (Planck) and WL (DES) surveys. The PCA method is ideal to investigate dark energy and modified gravity in a non-parametric way, which efficiently minimises the theoretical bias stemming from choosing \textit{ad hoc} functional forms for unknown functions.

We study dark energy and modified gravity separately. For dark energy equation-of-state, we find that SKA Phase 1 (2) can well constrain 3 and 5 eigenmodes of \( w(z) \) respectively. The errors on the best measured modes can be reduced to 0.04 and 0.023 for SKA1 and SKA2 respectively, making it possible to probe dark energy dynamics (Zhao et al. 2012). On the other hand, for modified gravity constraints, SKA1 (2) can constrain 7 (20) eigenmodes of \( \mu(k, z) \) respectively within
Figure 5: Eigensurfaces for the first three best constrained modes of $\mu$ after marginalisation over all other cosmological parameters. Top row: Planck + DES; Middle: Planck + DES + SKA1; Bottom: Planck + DES + SKA2.

10% sensitivity level. In particular 2 and 7 modes can be constrained within sub percent level using SKA1 and SKA2 respectively.

Imaging and redshift surveys are highly complementary when constraining cosmological parameters, especially for modified gravity models (Guzik et al. 2010; Song et al. 2011; Gaztañaga et al. 2012). The method developed in this work can be directly applied to future surveys of LSST (LSST Science Collaboration et al. 2009) and Euclid (Laureijs et al. 2011). For synergy between SKA and LSST and Euclid, see Bacon et al. (2015) and Kitching et al. (2015).

Acknowledgement:
GBZ is supported by Strategic Priority Research Program “The Emergence of Cosmological Structures” of the Chinese Academy of Sciences, Grant No. XDB09000000, by the 1000 Young Talents program in China, and by the 973 Program grant No. 2013CB837900, NSFC grant No. 11261140641, and CAS grant No. KJZD-EW-T01. All numeric calculations were performed on the SCIAMA2 supercomputer at University of Portsmouth. RM and MS are supported by the South African SKA Project and the National Research Foundation. DB and RM are supported by the UK Science & Technology Facilities Council (grant No. ST/K0090X/1).
References

Abdalla, F. et al. 2015, Proceedings of "Advancing Astrophysics with the Square Kilometre Array", PoS(AASKA14), 017
Anderson, L. et al. 2014, MNRAS, 441, 24
Asaba, S., Hikage, C., Koyama, K., Zhao, G.-B., Hojjati, A., & Pogosian, L. 2013, JCAP, 8, 29
Bacon, D. et al. 2015, Proceedings of "Advancing Astrophysics with the Square Kilometre Array", PoS(AASKA14), 145
Baker, T., Ferreira, P. G., & Skordis, C. 2013, Phys. Rev. D, 87, 024015
Bertschinger, E. & Zukin, P. 2008, Phys. Rev. D, 78, 024015
Bull, P. et al. 2015, Proceedings of "Advancing Astrophysics with the Square Kilometre Array", PoS(AASKA14), 024
Chevallier, M. & Polarski, D. 2001, International Journal of Modern Physics D, 10, 213
Clifton, T., Ferreira, P. G., Padilla, A., & Skordis, C. 2012, Phys. Rept., 513, 1
Crittenden, R. G., Pogosian, L., & Zhao, G.-B. 2009, JCAP, 12, 25
Crittenden, R. G., Zhao, G.-B., Pogosian, L., Samushia, L., & Zhang, X. 2012, JCAP, 2, 48
Gaztañaga, E., Eriksen, M., Crocce, M., Castander, F. J., Fosalba, P., Marti, P., Miquel, R., & Cabré, A. 2012, MNRAS, 422, 2904
Guzik, J., Jain, B., & Takada, M. 2010, Phys. Rev. D, 81, 023503
Hall, A., Bonvin, C., & Challinor, A. 2013, Phys. Rev. D, 87, 064026
Hojjati, A., Pogosian, L., & Zhao, G.-B. 2011, JCAP, 8, 5
Hu, W. & Sawicki, I. 2007, Phys. Rev. D, 76, 104043
Huterer, D. & Starkman, G. 2003, Physical Review Letters, 90, 031301
Kitching, T. et al. 2015, Proceedings of "Advancing Astrophysics with the Square Kilometre Array", PoS(AASKA14), 146
Laureijs, R. et al. 2011, arXiv1110.3193
Lewis, A., Challinor, A., & Lasenby, A. 2000, ApJ, 538, 473
Linder, E. V. 2003, Physical Review Letters, 90, 091301
LSST Science Collaboration et al. 2009, arXiv0912.0201
Perlmutter, S. et al. 1999, ApJ, 517, 565
Planck Collaboration et al. 2014, A & A, 571, A16
Raccanelli, A. et al. 2015, Proceedings of "Advancing Astrophysics with the Square Kilometre Array", PoS(AASKA14), 031
Riess, A. G. et al. 1998, AJ, 116, 1009
Santos, M. et al. 2015, Proceedings of "Advancing Astrophysics with the Square Kilometre Array", PoS(AASKA14), 021
Schölkopf, B., Smola, A. J., & Müller, K. R. 1998, Neural Computing, 10, 1299
Seo, H.-J. & Eisenstein, D. J. 2007, ApJ, 665, 14
Song, Y.-S., Zhao, G.-B., Bacon, D., Koyama, K., Nichol, R. C., & Pogosian, L. 2011, Phys. Rev. D, 84, 083523
Tegmark, M., Taylor, A. N., & Heavens, A. F. 1997, ApJ, 480, 22
Weinberg, D. H., Mortonson, M. J., Eisenstein, D. J., Hirata, C., Riess, A. G., & Rozo, E. 2013, Phys. Rept., 530, 87
Zhao, G.-B., Crittenden, R. G., Pogosian, L., & Zhang, X. 2012, Physical Review Letters, 109, 171301
Zhao, G.-B., Pogosian, L., Silvestri, A., & Zylberberg, J. 2009a, Physical Review Letters, 103, 241301
—. 2009b, Phys. Rev. D, 79, 083513