Turbulent jet flow generated downstream of a low temperature dielectric barrier atmospheric pressure plasma device

Richard D. Whalley & James L. Walsh

Flowing low temperature atmospheric pressure plasma devices have been used in many technological applications ranging from energy efficient combustion through to wound healing and cancer therapy. The generation of the plasma causes a sudden onset of turbulence in the inhomogeneous axisymmetric jet flow downstream of the plasma plume. The mean turbulent velocity fields are shown to be self-similar and independent of the applied voltage used to generate the plasma. It is proposed that the production of turbulence is related to a combination of the small-amplitude plasma induced body forces and gas heating causing perturbations in the unstable shear layers at the jet exit which grow as they move downstream, creating turbulence.

Low-temperature plasmas are strongly non-equilibrium systems, where the energy of electrons typically exceeds that of the ions and neutrals by several orders of magnitude; such conditions give rise to striking physical and chemical characteristics. Over the past half-century our growing understanding of these unique systems has underpinned some of the greatest achievements of the modern age, including semiconductor fabrication and energy efficient lighting. The generation of low-temperature plasma under atmospheric pressure conditions presents a new domain in plasma physics and enables the unique physical and chemical properties of the discharge to be accessed beyond the confines of a vacuum chamber.

Of the many different low temperature atmospheric pressure plasma devices currently under investigation, the dielectric barrier plasma plume stands alone due to its inherent ability to produce a plasma which is projected well beyond the confines of the generating electrodes. Such plasmas are typically created by ionizing a flowing noble gas within a capillary which exits into a background gas, creating an inhomogeneous axisymmetric jet flow. The plasma plume, rich in energetic metastable species and electrons, is free to interact with the background gas and in doing so initiates an abundance of dissociation, excitation and ionization reactions, ultimately yielding a rich reactive chemistry which is both accessible and non-thermal. These unique characteristics have been exploited across multiple diverse domains including nanoscale materials modification where reactive plasma species impinge on a surface to elicit changes in both functionality and morphology, energy efficient combustion where energetic plasma species provide new reaction pathways, and healthcare related applications including wound healing and cancer therapy, where reactive plasma species initiate biological responses in living tissues.

Underpinning all of these diverse applications is the reactive plasma chemistry. Uncovering a deeper physical and quantitative description of the velocity fields generated downstream of the discharge is the essential first step to improve our understanding of the production mechanisms of reactive chemical species at the plasma-gas interface. In order to address this complex and multifaceted challenge which spans the fields of plasma physics, fluid dynamics and non-equilibrium plasma chemistry, we report on the first quantitative measurements of the velocity fields generated downstream of a low temperature atmospheric pressure plasma plume.

Results and Discussion

The turbulent flow field of variable-density jets is characterized by the Froude number \((Fr)\), which is the ratio of momentum flux to buoyancy flux. The Froude number is defined as \(Fr = \frac{U_j^2 \rho_j}{gD(\rho_a - \rho_j)}\), where \(\rho_j\) is the density of the injected fluid, \(\rho_a\) is the density of the ambient fluid and \(g\) is the acceleration due to gravity. The
PIV seeding. The visible plasma ends is marked with a pink dot, and data in the laminar flow regime is omitted due to lack of turbulent flow fields observed in Fig. 1(b–d) are entirely consistent with all others in the literature10–13; the turbulent generated by the application of the plasma indicate a transition-to-turbulence from the instantaneous flow fields of the helium jet flow with plasma ignited, Fig. 1(b–d), where density fluctuations inlar. This is entirely consistent with observations at.

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Table 1. Nominal experimental conditions.

| Re     | Fr     | x/D   | f_0 (kHz) | U_m (m/s) |
|--------|--------|-------|-----------|-----------|
| 135 ± 5| 4,300 ± 75 | 20    | 27         | 17.5      |
| 260 ± 10| 15,450 ± 300 | 38    | 51         | 33.1      |
| 400 ± 25| 38,800 ± 1,200 | 60    | 81         | 52.6      |

Figure 1. Schlieren photography of (a) helium jet flow at Re = 135 and (b–d) helium jet flow at Re = 135 with plasma ignited at (b) 10kV, (c) 13kV and (d) 16kV.

vertical flow field is divided into three sections⁹, which are functions of downstream distance (x). First there is a region of pure jet behaviour which is dominated by momentum flux. This region begins at the jet exit (x/D = 0, where D is the inner diameter of the capillary) and extends as far as the dimensionless abscissa, X = (x/D) Fr = 0.5(p/ρ_j)_u ≈ 0.5. The pure jet transitions into a buoyant jet in an intermediary region which extends to ~10X. Beyond the intermediary region, the flow is dominated by buoyancy. The data presented here predominantly resides in the pure jet region where buoyancy is negligible: see Table 1 which details the downstream extent of the pure jet region, x/D.

Figure 1 shows Schlieren photography of the axisymmetric helium jet flow at a Reynolds number of Re = 135 (where U_m is the jet exit velocity and ν is the kinematic viscosity of helium). The jet flow begins at x/D = 0 and r is radial distance. In the absence of plasma (Fig. 1a) the helium jet flow remains laminar. This is entirely consistent with observations at Re = 260, and is broadly consistent with the flow fields at Re = 400, which begin to transition into a turbulent regime at x/D ≈ 25. These observations are in contrast to the instantaneous flow fields of the helium jet flow with plasma ignited, Fig. 1(b–d), where density fluctuations generated by the application of the plasma indicate a transition-to-turbulence from x/D ≈ 10. The developing turbulent flow fields observed in Fig. 1(b–d) are entirely consistent with all others in the literature10–13; the turbulent flow fields generated downstream of atmospheric plasma plumes have been qualitatively observed over a wide range of Reynolds number (135–840), applied voltage (8–30 kV peak-peak) and frequencies (125–50,000 Hz; St = f_0D/Um = 0.00012–0.035, where St = ~0.01D is the momentum thickness of the shear layers at the jet exit).

Figure 2 shows ensemble-averaged streamwise velocity of helium jet flow at Re = 260 with plasma ignited at 12–16 kV peak-peak. We observe that increasing the applied voltage does not increase the magnitude of the ensemble-averaged streamwise velocity within the turbulent flow region downstream of the discharge. This observation is entirely consistent with data at Re = 135 and 400. Note that throughout Fig. 2, the location where the visible plasma ends is marked with a pink dot, and data in the laminar flow regime is omitted due to lack of PIV seeding.

The ensemble-averaged electro-hydrodynamic force generated by guided streamers is ~5 × 10⁻⁶ Nm⁻³. Assuming, conservatively, that each guided streamer has a sheet length of ~250 μm, the increase in velocity due to the electro-hydrodynamic body force is ~0.003 – 0.025 U_m, over Re = 135–400. Further, the plasma increases the mean temperature of helium at the jet exit by ~10–30 degrees Celsius at 10–16 kV over Re = 135–400. Such a change in temperature causes an increase in jet exit velocity of ~0.03–0.09 U_m. Thus, gas heating and electro-hydrodynamic body forces do not significantly alter the mean velocity fields.

It is well known that the shear layers at the exit of an axisymmetric jet are highly unstable15,16. Small finite perturbations (~0.1 U_m) over a wide frequency range (St_d < 0.04) can grow exponentially in the unstable shear layers to transition jet flows into a turbulent regime from Re > 50017–20. Indeed, linear stability theory19 and many experimental investigations21 of homogeneous axisymmetric jet flow predict a dominant excitation frequency (f_0) at a Strouhal number of St_d ≈ 0.017. In this investigation at a Re = 260, a St_d ≈ 0.017 gives a dominant excitation
frequency of \( f_0 \sim 51 \text{ kHz} \) (see Table 1), which is close to the driving frequency of the sinusoidal waveform used to generate the plasma. More recently global instability modes in low density axisymmetric jets\(^2\) have been found to scale as \( fD^2/\nu \sim \text{Re}(D/\theta_0)^{1/2}(1 + (\rho_j/\rho_a)^{1/2}) \), entirely consistent with dominant frequencies on the order of 10's kHz for the helium jet flows discussed here, albeit with them located in the lower limit of this scaling law. Indeed, energy spectra of the discharge current show a dominant peak at the driving frequency of \( f \approx 50 \text{ kHz} \), accompanied by multiple high energy harmonics: see the (upper left) inset of Fig. 3. Thus, we propose that the sudden onset of turbulence observed within the flow fields (Fig. 2(b–d)) is generated by a combination of small-amplitude electro-hydrodynamic body forces and gas heating causing perturbations in the unstable shear layers at the jet exit, which become amplified as they travel downstream causing velocity fluctuations, Reynolds shear stresses, and thus the production of turbulence. Moreover, at higher applied voltages, the energy injected into the developing shear layers at the jet exit is increased, see for example the increase in energy around \( f \approx 50 \text{ kHz} \) in the (upper left) inset in Fig. 3, which causes the onset of turbulence closer to the jet exit; an observation well known within the literature\(^10\)–\(^13\), and one which is not accompanied by any significant increase in jet velocity, see Fig. 2.

Figure 2. Ensemble-averaged streamwise velocity of helium jet flow at \( \text{Re} = 260 \) with a plasma ignited at (a) 12 kV, (b) 14 kV and (c) 16 kV. Pink dot marks the end of the plasma plume.

Figure 3. Streamwise decay of the ensemble-averaged centreline velocity plotted against \( x^* \). Inset (bottom right) plotted against \( x/D \); 10 kV (\( \Delta \)), 11 kV (\( \nabla \)), 12 kV (\( \Phi \)), 13 kV (\( \varphi \)), 14 kV (\( \bigcirc \)), 15 kV (\( \bigodot \)), 16 kV (\( \odot \)); \( \text{Re} = 135 \) (black symbols), \( \text{Re} = 260 \) (red symbols), \( \text{Re} = 400 \) (red symbols). The green closed circles are helium jet flow without plasma at \( \text{Re} = 400 \) and \( Fr = 38,800 \). Inset (top left) shows power spectral density of current data at \( \text{Re} = 260 \); 12 kV (black line), 14 kV (red line), 16 kV (blue line). The data in the central part of the figure are down-sampled by a factor of two to ease viewing. The error bars show the uncertainty in obtaining the virtual origin.
The reduction in plasma plume length for higher applied voltages (see for example the locations of the pink dots in Fig. 2) is also due to the production of turbulence, mixing air into the helium jet flow and quenching the discharge.

Finally, we characterize the turbulent velocity fields generated by the atmospheric pressure plasma plumes. Figure 3 shows excellent collapse of the decay of the ensemble-averaged centreline velocity ($U_c$) when plotted with reduced streamwise coordinate, $x^* = (x - x_0)/d_e(x)$

$K_c \approx 0.12 \pm 0.017$ (to one standard deviation), which is in excellent agreement with inhomogeneous jet flow data in the literature$^{9,16,23,24}$. The error bars show the uncertainty in obtaining the virtual origin ($x_0$), which is ultimately due to the spatial resolution of the PIV setup. For comparative purposes, data from a helium jet flow at $Re = 400$ and $Fr = 643$ from Amielh et al.$^{24}$ (grey solid and dashed lines). For further comparison, the green closed circles in (d) are helium jet flow without plasma at $x^* = 70$: $Re = 400$ and $Fr = 38,800$.

Figure 4 shows the self-similar turbulence structure of the developing inhomogeneous jet flow. Djeridane et al.$^{27}$ showed that the axial evolution of local density within the pure jet region of helium and carbon dioxide axisymmetric jets scales as $\rho_1 \sim K_c (\rho_j/\rho_0)^{-0.85}(x - x_j)/D$, albeit over $Re \sim 10^3 - 10^4$. Here $K_c = 0.133^{27}$ is a constant, and $x_j$ is the length of the potential core of the jet, which is assumed to be negligibly small$^{28}$.

Figure 4 shows the self-similar turbulence structure of the developing inhomogeneous jet flow at $Re = 135$ (black symbols), $Re = 260$ (red symbols) and $Re = 400$ (blue symbols). With increasing distance from the jet exit, the radial profiles of the ensemble-averaged streamwise velocity (top) collapse to a single normalised exponential curve of the form: $\exp(-cr_{r_1/2})^2\ln(2)$, which is entirely consistent with all other turbulent jet data in the literature$^{9,16,23,24}$. The streamwise ($u'\bar{U}$; middle) and radial ($v'\bar{U}$; middle) velocity fluctuations, which represent local turbulence intensities, and the Reynolds shear stresses ($\overline{uv'}$; bottom), which indicates turbulence production, collapse when $x^* > 35$. The radial velocity fluctuations at $Re = 260$ and 400 follow a curve of the form: $3\sqrt{2}\overline{U} = 0.117 \exp(-0.4cr_{r_1/2})^2\ln(2)$, whilst the radial velocity fluctuations at $Re = 135$ follow: $3\sqrt{2}\overline{U} = 0.117 \exp(-0.4cr_{r_1/2})^2\ln(2)$. The data at $x^* = 25$ shows considerable scatter, indicating that the flow field is still developing into a self-similar structure at this streamwise distance (i.e. the velocity data does not collapse to a single curve). Furthermore, data for $Re = 135$, Fig. 4 (a, b; black symbols) does not collapse with data at higher $Re$. This is most likely due to the data at $Re = 135$ being located in the intermediate jet development region (see Table 1), which may not retain a self-similar turbulence structure$^{9,20}$. Generally, the data for $Re = 260$ and 400
show good agreement with the helium axisymmetric jet flow data of Amielh et al. 24 (grey solid and dashed lines). Further comparison is made with the helium jet flow data which is free from plasma at $Re = 400$, $x^* = 70$ (green closed circles), in Fig. 4(d). These data show that the radial profiles of the mean and higher order statistics collapse to the plasma data once scaled appropriately.

Summary
In this letter we report on the characteristics of an inhomogeneous axisymmetric turbulent jet flow generated downstream of a low temperature atmospheric pressure plasma plume. We have shown that the mean turbulent velocity fields of the jet flows under investigation are independent of applied voltage. Indeed, an order-of-magnitude analysis shows that the temperature and electro-hydrodynamic forces generated by the plasma have a negligible effect on the mean velocity fields. These results allow us to posit that the production of turbulence is due to a combination of the small-amplitude electro-hydrodynamic body forces and gas heating generating perturbations in the highly unstable shear layers at the jet exit, which grow as they move downstream, creating Reynolds shear stresses and thus the production of turbulence. Finally, and more broadly, by using a plasma as a unique excitation source, velocity measurements have been conducted in inhomogeneous axisymmetric turbulent jets at Reynolds numbers on the order of 100, which are one order of magnitude lower than any other study available within the literature. Even at such low Reynolds numbers, we have shown that the spatially developing velocity fields are turbulent and self-similar. Furthermore, we have shown that the developing self-similar turbulent velocity fields generated by the plasma are similar to the turbulent velocity fields which develop naturally (i.e. without a plasma) with increasing distance from the jet exit. These data provide vital information for the future development of low-temperature atmospheric pressure plasma plume devices and for the validation of associated computational models.

Methods
The low temperature atmospheric pressure plasma device investigated in this study is shown schematically in Fig. 5. The device consists of a quartz tube with an inner diameter ($D$) of 1.1 mm. The discharge was generated via a 10 mm wide copper electrode, which was wrapped around the outer circumference of the quartz tube and positioned 10 mm away from the jet exit. A custom-built power source applied a sinusoidal voltage waveform to the copper electrode at a voltage of 10–16 kV peak-to-peak at an AC driving frequency of 50 kHz. The applied voltage generated a stable plasma which protruded from the quartz tube within a flow of helium; in this single electrode
configuration the electrical circuit is completed via capacitive coupling to ground. An MKS mass flow controller regulated the flow of helium (99.996% purity) at 1, 2 or 3 Standard Litres per Minute (SLM). This provided a range in Reynolds number of \( Re = \frac{U_m D}{\nu_j} = 135–400 \) (where \( U_m \) is the jet exit velocity determined by mass continuity and \( \nu_j \) is the kinematic viscosity of helium). At a given standard flow rate, the jet exit Reynolds number (\( Re \)) monotonically decreased with increased applied voltage due to a small increase in mean fluid temperature at the jet exit (between 10–30 degrees Celsius increase above the ambient gas temperature with increasing applied voltage, measured by an Omega FOB100 fibre optic thermometer system). The nominal experimental conditions are shown in Table 1 with (±) range of \( Re \) as shown.

Global measurements of the velocity field were taken along the centreline of the jet with a time-resolved particle image velocimetry (PIV) system from TSI Incorporated. All measurements were conducted inside a closed chamber to ensure the helium jet flow was not influenced by any external drafts. The chamber had a cross-section of 1000 D × 1000 D and a height of 1500 D. Figure 6 shows a schematic representation of the experimental setup, showing the plasma plume device positioned in the laser sheet within the PIV enclosure. Olive oil with a nominal size of 1 μm was used to seed the air. The Stokes numbers of the seeding particles used throughout this study were <0.1. This ensured that the seeding particles followed the fluid flow closely with tracing errors being <1%. In total, 500 vector maps were acquired at a frequency of 500 Hz for each experiment. The velocity vectors were computed on a square grid with spatial resolution of 0.43 D using a recursive cross-correlation technique. Finally, the flow field was visualized using Schlieren photography with a Nikon D7000 camera at a shutter speed of 1/80 s; for details of this setup see Ghasemi et al.13.

References

1. Iza, F., Lee, J. K. & Kong, M. G. Electron kinetics in radio-frequency atmospheric-pressure microplasmas. *Physical Review Letters* **99**, 075004 (2007).
2. Shi, J. J. & Kong, M. G. Evolution of discharge structure in capacitive radio-frequency atmospheric microplasmas. *Physical Review Letters* **96**, 105009 (2006).
3. National Research Council. *Plasma Science: Advancing Knowledge in the National Interest (Physics 2010)* (National Academies Press, 2014).
4. Lu, X., Naidis, G. V., Laroussi, M. & Ostrick, K. Guided ionization waves: Theory and experiments. *Physics Reports* **540**, 123 (2014).
5. Labay, C. et al. Antibiotic-loaded polypropylene surgical meshes with suitable biological behaviour by plasma functionalization and polymerization. *Biomaterials* **71**, 132 (2015).
6. Kim, W., Do, H., Mungal, M. G. & Cappelli, M. A. Optimal discharge placement in plasma-assisted combustion of a methane jet in cross flow. *Combustion and Flame* **153**, 603 (2008).
7. Kong, M. G. et al. Plasma medicine: an introductory review. *New J. Phys.* **11**, 35, 115012 (2009).
8. Cheng, X. et al. The effect of tuning cold plasma composition on glioblastoma cell viability. *PLoS ONE* **9**, e98652 (2014).
9. Chen, C. J. & Rodi, C. J. Vertical turbulent buoyant jets - A review of experimental data (PERMAGRON Press, New York, 1980), The Science and Application of Heat and Mass Transfer.
10. Boselli, M. et al. High-speed multi-imaging of repetitive unipolar nanosecond-pulsed DBDs. *IEEE Transactions on Plasma Science* **42**, 2744, 6845351 (2014).
11. Bradley, J. W. et al. Schlieren photography of the outflow from a plasma jet. *IEEE Transactions on Plasma Science* **39**, 2312 (2011).
12. Papadopoulos, P. K. et al. Interpretation of the gas flow field modification induced by guided streamer (‘plasma bullet’) propagation. *Journal of Physics D: Applied Physics* **47**, 425203 (2014).
13. Ghasemi, M., Olszewski, P., Bradley, J. W. & Walsh, J. L. Interaction of multiple plasma plumes in an atmospheric pressure plasma jet array. *Journal of Physics D: Applied Physics* **46**, 052001 (2013).
14. Xiong, R., Xiong, Q., Nikiiforov, A. Y., Vanaaes, P. & Leys, C. Influence of helium mole fraction distribution on the properties of cold atmospheric pressure helium plasma jets. *Journal of Applied Physics* **112**, 033305 (2012).
15. Batchelor, G. K. & Gill, A. E. Analysis and instability of axisymmetric jets. *Journal of Fluid Mechanics* **14**, 529 (1962).
16. O’Neill, P., Soria, J. & Honnery, D. The stability of low Reynolds number round jets. *Experiments in Fluids* **36**, 473 (2004).
17. Vila, A. Experimental determination of the minimum Reynolds number for instability in a free jet. *Transactions of the ASME* **506** (1962).
18. Sato, H. & Sakao, F. An experimental investigation of the instability of a two-dimensional jet at low Reynolds number. *Journal of Fluid Mechanics* **20**, 337 (1964).
19. Michalke, A. On spatially growing disturbances in an inviscid shear layer. *Journal of Fluid Mechanics* **23**, 521 (1965).
20. Peacock, T., Bradley, E., Hertzberg, I. & Lee, Y. C. Forcing a planar jet flow using MEMS. *Experiments in Fluids* **37**, 22 (2004).
21. Gutmark, E. & Ho, C. M. Preferred modes and spreading rates of jets. *Physics of Fluids* **26**, 2932 (1983).
22. Hallberg, M. P. & Strykowski, P. J. On the universality of global modes in low-density axisymmetric jets. *Journal of Fluid Mechanics* **369**, 493 (2006).
23. Sato, H. & Sakao, F. An experimental investigation of the instability of a two-dimensional jet at low Reynolds number. *Journal of Fluid Mechanics* **20**, 337 (1964).
24. Amielh, M., Djeridane, T., Anselmet, F. & Fulachier, L. Velocity near-field of variable density turbulent jets. *International Journal of Heat and Mass Transfer* **39**, 2149 (1996).
25. Malmstrom, T. G., Kirkpatrick, A. T., Christensen, B. & Knappmiller, K. D. Centreline velocity decay measurements in low-Reynolds-number axisymmetric jets. *Journal of Fluid Mechanics* **246**, 363 (1997).
26. Hussein, H. J., Capp, S. J. & George, W. K. Velocity measurements in a high Reynolds number, momentum conserving, axisymmetric, turbulent jet. *Journal of Fluid Mechanics* **258**, 31 (1994).
27. Djeridane, T., Amielh, M., Anselmet, F. & Fulachier, L. Velocity turbulence properties in the near-field region of axisymmetric variable density jets. *Physics of Fluids* **8**, 1614 (1996).
28. Symons, E. P. & Labus, T. L. Experimental investigation of an axisymmetric fully developed laminar free jet, NASA Technical Note NASA TN D-6394 (1971).
29. So, R. M. & Aksoy, H. On vertical turbulent buoyant jets. *International Journal of Heat and Mass Transfer* **36**, 3187 (1993).
30. Tropea, C., Yarin, A. & Foss, J. *Springer Handbook of experimental fluid mechanics*. (Springer, New York, 2007).

**Acknowledgements**

J.L.W. would like to acknowledge the support of the Engineering and Physical Sciences Research Council (EPSRC), grant EP/J005894/1 and EP/N021347/1. R.D.W. would like to acknowledge the support of the NATO project AVT-254. Both authors would like to thank Dr. Martin Hyde of TSI for his assistance during the initial setup of the PIV system.

**Author Contributions**

J.L.W. and R.D.W. conceived the experiments, J.L.W. and R.D.W. conducted the experiments, J.L.W. and R.D.W. analysed the results. Both authors contributed to the compilation and review of the manuscript.

**Additional Information**

**Competing financial interests:** The authors declare no competing financial interests.

**How to cite this article:** Whalley, R. D. and Walsh, J. L. Turbulent jet flow generated downstream of a low temperature dielectric barrier atmospheric pressure plasma device. *Sci. Rep.* **6**, 31756; doi: 10.1038/srep31756 (2016).

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