Supplementary Information
Supporting Text. Nested Canalyzing Functions

Given a Boolean network $G(V, A)$, the value of each variable $v_i$ at time $t + 1$ is determined by the values of $k_i$ other variables $v_{i_1}, v_{i_2}, ..., v_{i_{k_i}}$ with a link to $v_i$ at time $t$ by the Boolean function $f_i$: $v_i(t + 1) = f_i(v_{i_1}(t), v_{i_2}(t), ..., v_{i_{k_i}}(t))$. The rule $f_i$ is called canalyzing on the input variable $v_{i_m}$ if there exist Boolean values, $I_m$ and $O_m$, such that

$$v_{i_m}(t) = I_m \rightarrow v_i(t + 1) = O_m.$$

Then, $I_m$ and $O_m$ are called the canalyzing and canalyzed values for the output variable $v_i$, respectively.

The notion of nested canalyzing functions (NCFs) was introduced in (Kauffman, et al., 2003), and they are a natural subset of canalyzing rules. It was inspired by the question of what happens in the noncanalyzing case: When a rule is not canalyzed by the value of the first input variable, is it canalyzed by one of the remaining input variables? This consecutive canalization test can be repeated for all inputs and therefore an NCFs to update $v_i$ can be represented as follows:

$$v_i(t + 1) = \begin{cases} O_1 & \text{if } v_{i_1}(t) = I_1 \\ O_2 & \text{if } v_{i_1}(t) \neq I_1 \text{ and } v_{i_2}(t) = I_2 \\ O_3 & \text{if } v_{i_1}(t) \neq I_1 \text{ and } v_{i_2}(t) \neq I_2 \text{ and } v_{i_3}(t) = I_3 \\ \vdots \\ O_{k_i} & \text{if } v_{i_1}(t) \neq I_1 \text{ and } \cdots \text{ and } v_{i_{k_i-1}}(t) \neq I_{k_i-1} \text{ and } v_{i_{k_i}}(t) = I_{k_i} \\ 1 - O_{k_i} & \text{otherwise} \end{cases}$$

Where all $I_m$ and $O_m \ (m = 1, 2, ..., k_i)$ denote the canalyzing and canalyzed values, respectively, and $O_{\text{default}} \neq O_{k_i}$. In addition, as in the previous studies (Kauffman, et al., 2003; Kauffman, et al., 2004), we independently and randomly specified $O_1, ..., O_{k_i}$ values with the probabilities

$$p(O_m = 1) = \frac{\exp(-2^{-m}\theta)}{1 + \exp(-2^{-m}\theta)}$$

where $\theta$ is a constant. On the other hand, the value of $I_m$ is deterministically specified by the value of $O_m$ and the sign of the interaction from $v_{i_m}$ to $v_i \ (m = 1, ..., k_i)$ as the following table.

| $O_m$ | Sign of the interaction from $v_{i_m}$ to $v_i$ | $I_m$ |
|-------|---------------------------------------------|------|
| 1     | Positive ($v_{i_m} \rightarrow v_i$)        | 1    |
| 1     | Negative ($v_{i_m} \rightarrow v_i$)        | 0    |
| 0     | Positive ($v_{i_m} \rightarrow v_i$)        | 0    |
| 0     | Negative ($v_{i_m} \rightarrow v_i$)        | 1    |
Supplementary Figures

Fig. S1. Analysis of the changes of the modularity and the robustness by edge-removal mutations in STF signaling network. The removal rate of edges was varied from 1% to 5% (More specifically, the numbers of removed edges were 5, 11, 16, 22, and 27, respectively, among a total of 557 edges). For each removal rate, 5,000 trials of edge-removal were examined. (a) Results of average changes of the modularity and the robustness against the removal rate of edges. Y-axis value and error bar represent the average and the standard deviation divided by the square root of the sample size (5000), respectively. Both average values were significantly larger than zero (All P-values <0.0001, using one-sample t-test). The one-sample t-test was valid because the average values were normally distributed (see Additional file 1: Fig. S4) and there were very few outliers (see Additional file 1: Fig. S7). (b)-(c) Relationship between the changes of the modularity and the robustness in the case that the removal rate is 1% and 2%, respectively. A significant negative relationship was observed (Correlation coefficients were -0.05254 and -0.022068, respectively, with all P-values <0.0001). This relationship was consistently observed for larger removal rates (Correlation coefficients when the removal rate of edge is 3%, 4%, and 5% were -0.03272 and, -0.04156, and -0.02795, respectively, with all P-values <0.0001). (d) A trend of correlation coefficients between the changes of the modularity and the robustness against the removal rate of edges.
Fig. S2. Analysis of the changes of the modularity and the robustness by edge-removal mutations in HIV-1 signaling network. The removal rate of edges was varied from 1% to 5% (More specifically, the numbers of removed edges were 3, 7, 11, 14, and 18, respectively, among a total of 368 edges). For each removal rate, 5,000 trials of edge-removal were examined. (a) Results of average changes of the modularity and the robustness against the removal rate of edges. Y-axis value and error bar represent the average and the standard deviation divided by the square root of the sample size (5000), respectively. Both average values were significantly larger than zero (All P-values <0.0001 using one-sample t-test). The one-sample t-test was valid because the average values were normally distributed (see Additional file 1: Fig. S5) and there were very few outliers (see Additional file 1: Fig. S8). (b)-(c) Relationship between the changes of the modularity and the robustness in the case that the removal rate is 1% and 2%, respectively. A significant negative relationship was observed (Correlation coefficients were -0.03867 and -0.05417, respectively with all P-values <0.0001). This relationship was consistently observed for larger removal rates (Correlation coefficients when the edge-removal rate is 3%, 4%, and 5% were -0.06862 and -0.05948, and -0.09733, respectively, with all P-values <0.0001). (d) A trend of correlation coefficients between the changes of the modularity and the robustness against the removal rate of edges.
**Fig. S3.** Analysis of normal distributions of averages of modularity changes and robustness changes in T-LGL network. (a)-(e) Results of the average of the modularity change with removal rates of 1% to 5%, respectively. (f)-(j) Results of the average of the robustness change with removal rates of 1% to 5%, respectively. In each subfigure, the average of the modularity or the robustness changes over 50 trials is computed, and this process was repeated 100 times to examine the distribution of the average variable. Kolmogorov-Smirnov test was run and all average values were normally distributed (All P-values > 0.10).
Fig. S4. Analysis of normal distributions of averages of modularity changes and robustness changes in STF network. (a)-(e) Results of the average of the modularity change with removal rates of 1% to 5%, respectively. (f)-(j) Results of the average of the robustness change with removal rates of 1% to 5%, respectively. In each subfigure, the average of the modularity or the robustness changes over 50 trials is computed, and this process was repeated 100 times to examine the distribution of the average variable. Kolmogorov-Smirnov test was run and all average values were normally distributed (All P-values > 0.10 except that P-value = 0.069 in (e)).
Fig. S5. Analysis of normal distributions of averages of modularity changes and robustness changes in HIV-1 network.

(a)-(e) Results of the average of the modularity change with removal rates of 1% to 5%, respectively. (f)-(j) Results of the average of the robustness change with removal rates of 1% to 5%, respectively. In each subfigure, the average of the modularity or the robustness changes over 50 trials is computed, and this process was repeated 100 times to examine the distribution of the average variable. Kolmogorov-Smirnov test was run and all average values were normally distributed (All P-values > 0.10 except that P-value = 0.053 in (d)).
Fig. S6. Analysis of outliers of averages of modularity changes and robustness changes in T-LGL network. (a)-(e) Results of the average of the modularity change with removal rates of 1% to 5%, respectively. (f)-(j) Results of the average of the robustness change with removal rates of 1% to 5%, respectively. In each subfigure, the average of the modularity or the robustness changes over 50 trials is computed, and this process was repeated 100 times to examine the distribution of the average variable. We examined outliers by a boxplot inspection and found no significant outliers in all subfigures except for (e), (h) and (j).
**Fig. S7.** Analysis of outliers of averages of modularity changes and robustness changes in STF network. (a)-(e) Results of the average of the modularity change with removal rates of 1% to 5%, respectively. (f)-(j) Results of the average of the robustness change with removal rates of 1% to 5%, respectively. In each subfigure, the average of the modularity or the robustness changes over 50 trials is computed, and this process was repeated 100 times to examine the distribution of the average variable. We examined outliers by a boxplot inspection and found no significant outliers in all subfigures except for (c), (i) and (j).
Fig. S8. Analysis of outliers of averages of modularity changes and robustness changes in HIV-1 network. (a)-(e) Results of the average of the modularity change with removal rates of 1% to 5%, respectively. (f)-(j) Results of the average of the robustness change with removal rates of 1% to 5%, respectively. In each subfigure, the average of the modularity or the robustness changes over 50 trials is computed, and this process was repeated 100 times to examine the distribution of the average variable. We examined outliers by a boxplot inspection and found no significant outliers in all subfigures except for (c) and (i).
Fig. S9. Relationship between the changes of the modularity and the robustness in T-LGL signaling network. (a)-(c) Results in the cases that the edge-removal rate is 3%, 4%, and 5%, respectively. Each plot is a result of 5,000 trials. Correlation coefficients of (a)-(c) were -0.30652, -0.30684, and -0.28626, respectively (All P-values <0.0001).
Fig. S10. Relationship between the changes of the modularity and the robustness in random networks. (a)-(c) Results of the random networks shuffled from T-LGL, STF, and HIV-1 signaling networks, respectively. In each subfigure, a set of 100 random networks were generated and 500 trials of edge-removals were tested for each network (Hence, each correlation coefficient was obtained over a total of 50,000 samples). We analyzed the relationship by varying the edge-removal rate from 1% to 5%. All cases showed significantly negative relationship (All P-values <0.0001).
Fig. S11. Relationship of each of the changes of the modularity and the robustness with the structural properties in STF signaling network. The removal rate was set 1%, and a total of 5,000 trials of removals were examined. (a)-(c) Relations of the change of modularity with edge-based degree, EBEW, and NuFBL, respectively. The change of modularity was significantly positively correlated with all structural properties (Correlation coefficients were 0.07621, 0.10084, and 0.07762, respectively, with all P-values<0.0001). (d)-(f) Relations of the change of robustness with edge-based degree, EBEW, and NuFBL, respectively. The change of robustness was significantly negatively correlated with all structural properties (Correlation coefficients were -0.03749, -0.11430, and -0.06860, respectively, with all P-values<0.0001).
Fig. S12. Relationship of each of the changes of the modularity and the robustness with the structural properties in HIV-1 signaling network. The removal rate was set 1%, and a total of 5,000 trials of removals were examined. (a)-(c) Relations of the change of modularity with edge-based degree, EBEW, and NuFBL, respectively. The change of modularity was significantly positively correlated with all structural properties (Correlation coefficients were 0.07549, 0.03526, and 0.05970, respectively, with all P-values<0.0001). (d)-(f) Relations of the change of robustness with edge-based degree, EBEW, and NuFBL, respectively. The change of robustness was significantly negatively correlated with all structural properties (Correlation coefficients were -0.07664, -0.04671, and -0.10621, respectively, with all P-values<0.0001).
Fig. S13. Relationship of each of the changes of the modularity and the robustness with the structural properties in random networks shuffled from T-LGL network. In each subfigure, a set of 100 random networks were generated and 500 trials of edge-removal were tested for each network (Hence, each correlation coefficient was obtained over a total of 50,000 samples). The removal rate was set 1%. (a)-(c) Relations of the change of modularity with edge-based degree, EBEW, and NuFBL, respectively. The change of modularity was significantly positively correlated with all structural properties (Correlation coefficients were 0.14388, 0.11878, and 0.10775, respectively, with all P-values<0.0001). (d)-(f) Relations of the change of robustness with edge-based degree, EBEW, and NuFBL, respectively. The change of robustness was significantly negatively correlated with all structural properties (Correlation coefficients were -0.14851, -0.11281, and -0.08690, respectively, with all P-values<0.0001).
Fig. S14. Relationship of each of the changes of the modularity and the robustness with the structural properties in random networks shuffled from STF network. In each subfigure, a set of 100 random networks were generated and 500 trials of edge-removal were tested for each network (Hence, each correlation coefficient was obtained over a total of 50,000 samples). The removal rate was set 1%. (a)-(c) Relations of the change of modularity with edge-based degree, EBEW, and NuFBL, respectively. The change of modularity was significantly positively correlated with all structural properties (Correlation coefficients were 0.03228, 0.01516, and 0.01062, respectively, with all P-values<0.0001). (d)-(f) Relations of the change of robustness with edge-based degree, EBEW, and NuFBL, respectively. The change of robustness was significantly negatively correlated with all structural properties (Correlation coefficients were -0.07121, -0.05301, and -0.04716, respectively, with all P-values<0.0001).
Fig. S15. Relationship of each of the changes of the modularity and the robustness with the structural properties in random networks shuffled from HIV-1 network. In each subfigure, a set of 100 random networks were generated and 500 trials of edge-removal were tested for each network (Hence, each correlation coefficient was obtained over a total of 50,000 samples). The removal rate was set 1%. (a)-(c) Relations of the change of modularity with edge-based degree, EBEW, and NuFBL, respectively. The change of modularity was significantly positively correlated with all structural properties (Correlation coefficients were 0.11393, 0.04112, and 0.04064, respectively, with all P-values<0.0001). (d)-(f) Relations of the change of robustness with edge-based degree, EBEW, and NuFBL, respectively. The change of robustness was significantly negatively correlated with all structural properties (Correlation coefficients were -0.08353, -0.08649, and -0.09906, respectively, with all P-values<0.0001).
Fig. S16. Topological distributions of High-MI/High-RD edges and their incident nodes in STF signaling network. (a)-(b) Distributions of High-MI and High-RD edges, respectively, and their incident nodes. (c)-(d) Subgraphs with respect to High-MI-incident and High-RD-incident nodes, respectively. Red link and yellow node represent High-MI edge and High-MI-incident node, respectively, in both (a) and (c), whereas they represent High-RD edge and High-RD-incident node, respectively, in both (b) and (d).
**Fig. S17.** Topological distributions of High-MI/High-RD edges and their incident nodes in HIV-1 signaling network. (a)–(b) Distributions of High-MI and High-RD edges, respectively, and their incident nodes. (c)–(d) Subgraphs with respect to High-MI-incident and High-RD-incident nodes, respectively. Red link and yellow node represent High-MI edge and High-MI-incident node, respectively, in both (a) and (c), whereas they represent High-RD edge and High-RD-incident node, respectively, in both (b) and (d).
Fig. S18. Edge-removal analysis for edgetic drug discovery in STF signaling network. The arrows and bar-headed lines represent positive and negative interactions, respectively. Line thickness is proportional to the inclusion frequency of the interaction in top-\(K\) edge sets ranked in a decreasing order of the robustness change among 5000 trials of edge-removal mutations with 1\% removal rate. The interaction (\(IP3R1 \rightarrow Ca\)) was observed 17 times in top-\(K\) edge sets (\(K\) was chosen to 18).
**Fig. S19.** Edge-removal analysis for edgetic drug discovery in HIV-1 signaling network. The arrows and bar-headed lines represent positive and negative interactions, respectively. Line thickness is proportional to the inclusion frequency of the interaction in top-$K$ edge sets ranked in a decreasing order of the robustness change among 5000 trials of edge-removal mutations with 1% removal rate. The interactions $(gp41 \rightarrow CD28)$ and $(PI3K \rightarrow PIP3)$ were observed 6 and 3 times, respectively, in top-$K$ edge sets ($K$ was chosen to 16).
**Table. S1.** GO analysis results between High-MI-incident/High-RD-incident group and the rest of genes in STF network. All P-values were calculated by using Bonferroni test.

| Type of GO analysis | GO term                                                                 | High-MI-incident (%) | The rest of genes (%) | P-value     |
|---------------------|-------------------------------------------------------------------------|----------------------|-----------------------|-------------|
| Modularity change   | Protein kinase activator activity                                        | 75.00                | 25.00                 | 360.0E-6    |
|                     | Negative regulation of cysteine-type endopeptidase activity              | 66.84                | 40.11                 | 1.1E-6      |
|                     | Response to mechanical stimulus                                          | 74.13                | 37.07                 | 93.0E-9     |
|                     | Activation of immune response                                            | 75.09                | 27.66                 | 120.0E-18   |
|                     | Protein phosphatase binding                                              | 84.82                | 21.21                 | 7.1E-9      |
|                     | Mitogen-activated protein kinase kinase binding                          | 75.00                | 25.00                 | 1.9E-6      |
|                     | Growth factor receptor binding                                           | 76.73                | 30.69                 | 50.0E-6     |
|                     | Insulin receptor binding                                                 | 89.82                | 17.96                 | 450.0E-9    |
|                     | GO term                                                                 | High-RD-incident (%) | The rest of genes (%) | P-value     |
| Robustness change   | Rho guanyl-nucleotide exchange factor activity                           | 75.00                | 25.00                 | 760.0E-6    |
|                     | Protein serine/threonine/tyrosine kinase activity                        | 62.50                | 37.50                 | 44.0E-12    |
|                     | Cellular response to carbohydrate stimulus                               | 66.67                | 33.33                 | 47.0E-6     |
|                     | Response to epidermal growth factor                                      | 60.00                | 40.00                 | 1.4E-6      |
|                     | Antigen receptor-mediated signaling pathway                               | 72.73                | 27.27                 | 42.0E-9     |
|                     | Lipopolysaccharide-mediated signaling pathway                            | 75.00                | 25.00                 | 190.0E-6    |
|                     | Immune response-activating cell surface receptor signaling pathway       | 71.70                | 31.37                 | 55.0E-18    |
|                     | Neurotrophin TRK receptor signaling pathway                              | 64.60                | 43.07                 | 8.5E-6      |
Table. S2. GO analysis results between High-MI-incident/High-RD-incident group and the rest of genes in HIV-1 network. All P-values were calculated by using Bonferroni test.

| Type of GO analysis | GO term                                                    | High-MI-incident (%) | The rest of genes (%) | P-value     |
|---------------------|------------------------------------------------------------|----------------------|-----------------------|-------------|
| Modularity change   | Negative regulation of kinase activity                    | 61.54                | 38.46                 | 720.0E-12   |
|                     | Virus receptor activity                                    | 75.00                | 25.00                 | 470.0E-6    |
|                     | Regulation of defense response to virus                   | 60.00                | 40.00                 | 100.0E-6    |
|                     | Positive regulation of immune response                   | 64.34                | 39.06                 | 560.0E-36   |
|                     | Response to growth hormone                               | 66.67                | 33.33                 | 45.0E-9     |
|                     | Phosphatase binding                                       | 63.64                | 36.36                 | 510.0E-12   |
|                     | Phosphotyrosine binding                                   | 60.00                | 40.00                 | 5.5E-9      |
|                     | Protein phosphatase binding                              | 66.67                | 33.33                 | 7.9E-9      |
|                      | Robustness change                                         |                      |                       |             |
|                     | Receptor signaling protein serine/threonine kinase activity | 72.73                | 27.27                 | 2.5E-12     |
|                     | MAP kinase kinase kinase activity                         | 75.00                | 25.00                 | 7.0E-6      |
|                     | Response to axon injury                                  | 75.00                | 25.00                 | 550.0E-6    |
|                     | Mast cell activation involved in immune response          | 61.39                | 46.04                 | 200.0E-9    |
|                     | Stimulatory C-type lectin receptor signaling pathway      | 60.00                | 40.00                 | 180.0E-12   |
|                     | Lipopolysaccharide-mediated signaling pathway             | 60.00                | 40.00                 | 11.0E-6     |
|                     | Negative regulation of ERBB signaling pathway            | 75.00                | 25.00                 | 91.0E-6     |
|                     | Negative regulation of epidermal growth factor receptor signaling pathway | 75.00                | 25.00                 | 83.0E-6     |
References

Kauffman, S., et al. (2003) Random Boolean network models and the yeast transcriptional network, *P Natl Acad Sci USA*, **100**, 14796-14799.

Kauffman, S., et al. (2004) Genetic networks with canalyzing Boolean rules are always stable, *P Natl Acad Sci USA*, **101**, 17102-17107.