Spin-Current-Induced Charge Accumulation and Electric Current in Semiconductor Nanostructures with Rashba Spin-Orbit Coupling

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We demonstrate that the flow of a longitudinal spin current with different spin polarization will induce different patterns of charge accumulation in a two-terminal strip, or electric current distribution in a four-terminal Hall-bar structure, of two-dimensional electron gas with Rashba spin-orbit coupling (RSOC). For an in-plane polarized spin current, charges will accumulate either by the two lateral edges or around the center of the strip structure while, for an out-of-plane polarized spin current, charge densities will show opposite signs by the two lateral edges leading to a Hall voltage. Our calculation offers a new route to experimentally detect or differentiate pure spin currents with various spin polarization.

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Semiconductor spintronics has achieved remarkable success in the past decade and is still progressing rapidly. And spin-orbit science and engineering, which allow for electrical manipulation of spin polarization and spin currents in nonmagnetic semiconductors, is one of the key steps to implement spintronic devices. Utilizing spin-orbit coupling, various schemes were proposed to generate pure spin currents while to detect pure spin currents remains a challenge from either experimental or theoretical aspect. The detection of spin currents often involves spin accumulation or electrical effects, despite quantum interferences by optical means also reported. For example, spin accumulation induced by spin current near the boundaries has been detected in both n- and p-doped semiconductor systems experimentally and Hall voltage resulted from the reciprocal extrinsic spin Hall effect was observed in diffusive metallic conductors. Recently it was reported that an optically injected spin current flowing through a Hall-bar semiconductor can generate either in-ward or out-ward electric currents while the Hall voltage remains zero. This observation renders a manifestations of the tensor-like nature of the spin current, which means that both the spin polarization and the direction of motion are decisive factors in producing physically observable effects.

The electrical detection of spin currents has reduced complexities in practice and thus is potentially more applicable. Whereas a fundamental problem of theoretically studying the electrical effects resulted from spin currents, is the difficulties to incorporate the concept of spin current into a theoretical formalism, for reasons like the ambiguous definition of spin currents under certain circumstances. In this Letter we investigate such effects in a mesoscopic system of spin-orbit-coupled two-dimensional gas (2DEG) with ideal leads which connect several special electron reservoirs. Generation of the spin current is simulated phenomenologically by introducing spin-dependent chemical potentials within each electron reservoir. These chemical potentials are tuned separately for each spin component to produce independent potential gradients, so that electrons with opposite spins are driven to move in opposite directions through the spin-conserved leads and the spin-orbit-coupled central region. It must be emphasized that the aim of this phenomenological simulation is to capture only the general and essential features of the spin current flow, without bothering about the details of the method in its generation and injection, and this is justified as long as we keep our focus on the electrical effects that are led by or intimately related to the circulation of the spin current.

We demonstrate spin-current-induced electrical effects by showing charge accumulation induced in a strip structure and the electric current distribution in a corresponding Hall-bar structure. The Landauer-Büttiker-Keldysh formalism is used in our calculations, which is a quantum-in-nature approach and has extensive applications. The total Hamiltonian of the central region is

$$H_C = H_0 + H_{SO},$$

where $H_0 = \frac{\hbar^2 k^2}{2 m} + V_0$ is the kinetic energy plus the hard-wall confining potential $V_0$, $m^*$ is the effective electron mass, and $H_{SO} = -\alpha (\mathbf{k} \times \sigma) \cdot z$, with $\alpha$ the strength of Rashba spin-orbit coupling (RSOC), $\mathbf{k}$ the wave vector, $\sigma$ the vector composed of Pauli’s matrices, and $\hat{z}$ the unit vector perpendicular to the plane of the 2DEG. After discretizing $H_C$ with the tight-binding approximation and transforming it into the spin bases which are the eigenstates (denoted by $\chi_\mu$ or $\chi_\nu$, where $\mu, \nu = \uparrow$ or $\downarrow$) of $\hat{r} \cdot \sigma$, where $\hat{r}$ is the orientation of spin polarization under consideration, we have

$$H_C = \sum_{<i,j>} \sum_{\mu, \nu} t_{ij}^{\mu\nu} c_{i\mu}^{\dagger} c_{j\nu}$$

where $c^{\dagger}$ and $c$ are the creation and annihilation operators of electrons at sites $i$($j$) with spin $\mu$($\nu$) and $< \cdots >$
FIG. 1: Spin-current-induced charge distributions in a 200nm×100nm strip, where the spin current is polarized along \( \hat{y} \) and the distributions are displayed after the spin-independent background distribution (when \( \alpha = 0 \) has been subtracted from). (a) the image of charge distribution when \( \alpha = -6.1 \times 10^{-12} \text{eVm} \). (b) the image of charge distribution when \( \alpha = 6.1 \times 10^{-12} \text{eVm} \). (c) and (d) the averaged (in terms of the longitudinal dimension) charge distributions along the narrow side of the sample, comparing different cases with \( \alpha \) having the same sign (negative for plot (c) and positive for plot (d)) but increasing magnitudes.

Our present study focuses on electrical effects resulted from spin current with spin polarization oriented in plane (referred to as \( \hat{y} \) henceforth) which is perpendicular to the direction of motion (referred to as \( \hat{x} \) henceforth) of electron spin. When a spin current with \( \hat{y} \)-spin-polarization is flowing through a strip, depending upon the sign of the RSOC \( \alpha \), which stands for whether the velocity, the spin polarization and the gradient of potential for the RSOC satisfy the left-hand or right-hand chirality, the electric charges will accumulate either near the lateral edges or around the middle of stripe, as shown in Fig. 1. In this figure, two equal-magnitude +\( \hat{y} \)/−\( \hat{y} \)-spin-polarized currents are driven in the direction +\( \hat{x} \)/−\( \hat{x} \) by the spin-dependent chemical potentials \( \epsilon^\mu_{\pm x} = \pm \text{sign}(\mu)0.1t_0 \) through a 40×20 lattice with the Fermi Energy \( E_f = 0.1t_0 \), which is measured from the bottom of the conduction band and is small enough to ensure the parabolic energy-momentum dispersion in the tight-binding approximation, and \( \alpha = -6.1 \times 10^{-12} \text{eVm} \) or \( t_{SO}^R = -0.02t_0 \) in Fig. 1(a), and \( \alpha = +6.1 \times 10^{-12} \text{eVm} \) or \( t_{SO}^R = +0.02t_0 \) in Fig. 1(b), respectively. It is easy to identify that the charges of carriers accumulate by the two lateral edges in the former case and at the middle part in the latter one. This is further manifested by a comparison of Fig. 1(c) and Fig. 1(d), where the averaged charge densities with \( \pm \alpha \) are plotted. For a negative \( \alpha \), increased magnitude will lead to increased accumulation by the edges, while for a positive \( \alpha \), the same trend happens at the middle. It should be noted that since we do not consider any dissipation mechanisms inside our samples, these accumulations should be interpreted as an effect purely due to quantum coherent transport.
To show physical consequences of charge accumulation in a strip structure, we calculated electric current distributions in a Hall-bar structure where two additional leads are symmetrically attached to the two lateral sides of the original strip as illustrated in Fig. 1. The direction and magnitude of local current density are indicated by the orientation and length of arrows, respectively. The transverse electric currents are both flowing outward in plot (a), where \( \alpha = -6.1 \times 10^{-12} \text{eV} \) and the ratio of the total induced electric current to the circulating spin current \( I_e/I_s = 2.57 \times 10^{-12} \frac{e\nu}{\hbar^2} \), or both flowing inward in plot (b), where \( \alpha = 6.1 \times 10^{-12} \text{eV} \) and \( I_e/I_s = 1.14 \times 10^{-2} \frac{e\nu}{\hbar^2} \).

![FIG. 2: Charge current distributions after two additional leads are connected to the lateral edges of the strip in Fig. 1. The direction and magnitude of local current density are indicated by the orientation and length of arrows, respectively. The transverse electric currents are both flowing outward in plot (a), where \( \alpha = -6.1 \times 10^{-12} \text{eV} \) and the ratio of the total induced electric current to the circulating spin current \( I_e/I_s = 2.57 \times 10^{-12} \frac{e\nu}{\hbar^2} \), or both flowing inward in plot (b), where \( \alpha = 6.1 \times 10^{-12} \text{eV} \) and \( I_e/I_s = 1.14 \times 10^{-2} \frac{e\nu}{\hbar^2} \).](image)

So far we have mainly discussed the charge density and the electric current distribution induced by a spin current with in-plane spin polarization (along \( \hat{y} \)). Yet a tensor as a spin current is in essence, it is also worthwhile to investigate the spin current with different configurations of spin polarization and velocity. Without losing the generality, we concentrate on three cases of spin along \( \hat{x} \), \( \hat{y} \) and \( \hat{z} \), respectively. From the study of these special cases, the generic result for a spin current with arbitrary spin polarization can be derived, and also maximum symmetries can be observed therein. Since one of these cases with \( \hat{y} \)-spin-polarization has been presented already, we show the charge distributions induced in other two cases in Fig. 3. Compared with the induced charge distribution shown in Fig. 1(b), which is calculated with all the same parameters except for the spin polarization of the spin current, the induced charge distributions in Fig. 3(a) and (b) show clear differences in terms of the spacial symmetries they possess, that is the \( C_{2v} \) symmetry in the case when spin polarized along \( \hat{y} \), the \( C_2 \) symmetry when spin polarized along \( \hat{x} \), and the \( C_s \) symmetry when spin polarized along \( \hat{z} \). This is because the underlying system is invariant under each operation of the \( C_{2v} \) space group combined with an appropriate unitary transformation in the spin space, while in order that the circulating spin current is also invariant under that combination of transformations, the valid space-group operations will be limited into a subgroup of \( C_{2v} \) (\( C_{2v} \) itself in the \( \hat{y} \)-spin-polarization case, and \( C_2 \) or \( C_s \) in the \( \hat{x} \) or \( \hat{z} \)-spin-polarization case respectively), accordingly the charge distributions induced by different spin currents will exhibit different symmetry properties. Also it is easy to infer that the electric current distributions or any other electric effect induced by a corresponding spin current will display the same spacial symmetry as long as the structural symmetry of the system is preserved, which is actually a general yet rigorous limitation and.

![FIG. 3: Spin-current-induced charge distributions in a 200nm \times 100nm strip, where the spin current is polarized along \( \hat{x} \) in (a) and along \( \hat{z} \) in (b). \( \alpha = 6.1 \times 10^{-12} \text{eV} \) and the distributions are displayed after the spin-independent background distribution has been subtracted from.](image)
has been justified in all our calculations that are shown or not shown here.

Moreover, the relevance of the spin polarization of spin current to the induced charge accumulation also lies in the differences between the average distributions along the transverse of the strip resulted from spin currents which are polarized in different directions. In particular, the transverse of the strip resulted from spin currents to the induced charge accumulation also lies in or not shown here.

The reciprocal version of the spin Hall effect, which is closely related to as well as consistent with the average will have opposite signs near the two lateral edges, when the spin current is polarized along $\hat{y}$. When the spin current is polarized along $\hat{z}$, however, it can be observed from Fig 3(b) that the charge accumulation on average will have opposite signs near the two lateral edges, which is closely related to as well as consistent with the reciprocal version of the spin Hall effect, and was reported to be observed in platinum wires. In another case that the spin current with $\hat{z}$-spin-polarization is considered, the pattern of the charge accumulation (shown in Fig 3(a)) is more complex in the sense that there are reversed accumulating trends at the two sides of the transverse plane passing through the symmetric center, which is determined by the $C_2$ symmetry of this system mentioned above. While after average has been taken over the longitudinal dimension, it can be reasonably expected that the opposite accumulations of two halves will tend to cancel each other and produce a weakened net effect with symmetrical distribution about the transversal center. In contrast to that in the $\hat{y}$-spin-polarized case, in either case with the $\hat{x}$- or $\hat{z}$-spin-polarization, the averaged distribution along the traverse does not change under the reversal of the sign of $\alpha$. Besides, we notice that the electric effects induced by different spin currents are actually contributed by different ranks of power with respect to $\alpha$, which is also manifested when the sign of $\alpha$ is reversed. Specifically, when the spin current is polarized along $\hat{x}$ or $\hat{y}$, it is mainly the linear $\alpha$ that is responsible for the induced electric effects, while in the $\hat{z}$-spin-polarized case, it is the second rank, i.e. $\alpha^2$, playing the role.

We conclude this letter by evaluating the accessibility of an experimental observation to the electrical patterns investigated here. From the data plotted in Fig 1(c), we estimate roughly the electrostatic potential difference $\Delta V$ to be of order 0.1mV between either of the peaks and the valley of the charge distribution as long as $\alpha > 3 \times 10^{-12} \text{eV}$. And in a realistic semiconductor quantum well with the Fermi energy typically being tens of meV, the electronic potential difference will increase to at least several meV or tens of Kelvins subject to increased RSOE strength. This implies that the temperature requirement for observing these patterns can be well satisfied within current experimental conditions. Regarding these features as well as the sample size, we propose the use of Kelvin probe force microscopy in observing the charge accumulation predicted here. On the other hand, we point out that the present work may also account for a recent experimental observation of the spin-current-induced electric currents, which possess the key features exhibited in Fig 1 and Fig 2 that is, there is no Hall voltage while the electric currents circulate through $x$-channels to $y$-channels. And quantitatively the experiment is consistent with the calculated ratio of the induced charge current to the spin current captioned in Fig 1. In short, the spin current with in-plane spin polarization may produce measurable charge accumulations or electric currents with a novel behavior, and the underlying effects may open a promising way to the electrical detection of spin currents.

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