Coverage Probability of STAR-RIS assisted Massive MIMO systems with Correlation and Phase Errors

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Abstract—In this paper, we investigate a simultaneous transmitting and reflecting reconfigurable intelligent surface (STAR-RIS) assisting a massive multiple-input multiple-output (mMIMO) system. In particular, we derive a closed-form expression for the coverage probability of a STAR-RIS assisted mMIMO system while accounting for correlated fading and phase-shift errors. Notably, the phase configuration takes place at every several coherence intervals by optimizing the coverage probability since the latter depends on statistical channel state information (CSI) in terms of large-scale statistics. As a result, we achieve a reduced complexity and overhead for the optimization of passive beamforming, which are increased in the case of STAR-RIS networks with instantaneous CSI. Numerical results corroborate our analysis, shed light on interesting properties such as the impact of the number of RIS elements and the effect of phase errors, along with affirming the superiority of STAR-RIS against reflective-only RIS.

Index Terms—Reconfigurable intelligent surface (RIS), simultaneous transmission and reflection, spatial correlation, coverage probability, 6G networks.

I. INTRODUCTION

Reconfigurable intelligent surface (RIS) is a promising technology, enabling a smart radio environment (SRE) to meet the challenges of sixth-generation (6G) wireless networks [1]. It consists of a number of low-cost nearly passive elements that can modify the phase shifts and even the amplitude of the impinging signals to realize an SRE through a backhaul controller. RIS favorable characteristics have led recently the research interest in meeting certain significant targets such as maximization of the spectral and energy efficiencies [2], [3], and maximization of the coverage probability [4], [5]. Notably, given that 6G will be built upon existing technologies in 5G such as massive multiple-input multiple-output (mMIMO) systems, the latter suggests a promising architecture for amalgamation with RIS [6].

Thus far, there has been a considerable amount of research on RISs. However, most of the existing works in the literature assume independent Rayleigh fading such as [3], [7]. In contrast, in [5], it was shown that RIS correlation should be taken into account in practice. On this ground, several recent research efforts have considered RIS correlation in their analysis [5], [8]. Furthermore, aiming at realistic modeling, many works have taken into account phase-shift errors coming from the finite precision of phase-shifts configuration [2], [10]. Recent advancements on metasurfaces have brought to the forefront the concept of simultaneous transmitting and reflecting RISs (STAR-RISs). In particular, the STAR-RIS can provide a full space coverage by not only reflecting in the half space, but also refracting to space behind the RIS [11], [12]. In particular, in [11], a general hardware model and two-channel models for the near-field region and the far-field region of STAR-RIS have been presented while showing that their diversity gain and coverage are greater than conventional RIS (i.e. reflective-only RIS) assisted systems. Moreover, in [12], three operating protocols for STAR-RIS were suggested, which are known as energy splitting (ES), mode switching (MS), and time switching (TS). However, none of the existing works on STAR-RIS have considered correlated fading, phase errors, and mMIMO systems.

Against the above background, we provide in closed form the only work obtaining the coverage probability for STAR-RIS assisted mMIMO systems with practical channel and phase models. In particular, contrary to existing works on STAR-RIS such as [11], [12], we formulate a model that embodies correlated fading and phase errors to identify the realistic prospects of STAR-RIS before its final implementation. In this respect, we derive the coverage probability for mMIMO systems for both ES and MS protocols. Especially, compared to [11], which assumed a single-antenna transmitter, and required no special phase-shifts optimization, we also consider a large number of antennas at the base station (BS). For this reason, we follow the methodology in [2], [5] based on statistical channel state information (CSI) to optimize the passive (reflecting and refracting) beamforming matrix (PBM) of each user equipment (UE) at every several coherence intervals, which brings lower overhead compared to optimizations relying on instantaneous CSI. To the best of our knowledge, this is the only work on STAR-RIS, where both beamforming matrices for reflection and refraction are optimized based on statistical CSI, and thereby reducing the amount of required overhead, which can be considered as one of the main challenges for STAR-RIS.

This section presents the signal and system models of the STAR-RIS assisted system.

A. Signal Model

Regarding the description of the signal model of the STAR-RIS, let $\sigma_n$ describe the incident signal on element $n \in \mathcal{N}$, where $\mathcal{N} = \{1, \ldots, N\}$ is the set of RIS elements. Two independent coefficients, denoted as the transmission and the reflection coefficients, configure the transmitted and reflected signals in respective modes. Especially, the transmitted $(t)$ and reflected $(r)$ signals by the $n$th element can be modelled as $t_n = (\sqrt{\beta_n} e^{j\phi_n}) s_n$ and $r_n = (\sqrt{\beta_n} e^{j\phi_n}) s_n$, respectively, where $\beta_n \in [0, 1]$ and $\phi_n \in [0, 2\pi]$ express the independent amplitude and phase-shift response of the $n$th element, and $k \in \{t, r\}$ corresponds to the UE found in the transmission $(t)$...
or reflection (r) region \(\Pi\). Note that the choice of \(\phi_t^r\) and \(\phi_r^r\) is independent from each other, but the amplitude adjustments are correlated based on the law of energy conservation as
\[
\beta_t^r + \beta_r^r = 1, \forall n \in \mathcal{N}.
\]

**Operation Protocols:** Herein, we present briefly the main points of the ES/MS protocols [12]. The study of the TS protocol is left for future work.

**ES protocol:** All RIS elements serve simultaneously \(t\) and \(r\) UEs, and the corresponding PBM for \(k \in \{t, r\}\) is expressed as
\[
\Phi_k^{ES} = \text{diag}(\sqrt{\beta_t^k e^{j\phi_t^k}}, \ldots, \sqrt{\beta_r^k e^{j\phi_r^k}}) \in \mathbb{C}^{N \times N},
\]
where \(\beta_t^k, \beta_r^k \in [0, 1], \beta_t^k + \beta_r^k = 1, \) and \(\phi_t^k, \phi_r^k \in [0, 2\pi), \forall n \in \mathcal{N}.
\]

**MS protocol:** The elements are divided into two groups of \(N_t\) and \(N_r\) elements serving UE \(t\) or \(r\), respectively, i.e., \(N_t + N_r = N\). In such case, the PBM for \(k \in \{t, r\}\) is
\[
\Phi_k^{MS} = \text{diag}(\sqrt{\beta_t^k e^{j\phi_t^k}}, \ldots, \sqrt{\beta_r^k e^{j\phi_r^k}}) \in \mathbb{C}^{N \times N},
\]
where \(\beta_t^k, \beta_r^k \in [0, 1], \beta_t^k + \beta_r^k = 1, \) and \(\phi_t^k, \phi_r^k \in [0, 2\pi), \forall n \in \mathcal{N}.
\]

1) **RIS correlation:** Instead of assuming independent Rayleigh fading as in existing STAR-RIS works [11, 12], we consider spatial correlation, appearing in practice [9]. Hence, the channel vector between the RIS and UE \(k \in \{t, r\}\) can be written as
\[
h_k = \sqrt{\beta_k} R_k^{1/2} \Phi_k z_k,
\]
where \(\beta_k\) expresses the path-loss, and \(R_k \in \mathbb{C}^{N \times N}\) with \(\text{tr}(R_k) = N\) expresses the deterministic Hermitian-symmetric positive semi-definite correlation matrix at the RIS. In particular, if \(N \sim N_H N_V\) elements with \(N_H\) the number of elements per row and \(N_V\) the number of elements per column, while \(d_H\) and \(d_V\) are horizontal and vertical dimensions of each elements, the \((i, j)\)th element of the RIS correlation is given by
\[
r_{ij} = d_H d_V \sin(2\pi u_i - u_j) / \lambda,
\]
where \(u_i = [0, \ldots, (i - 1) N_H d_H, (i - 1) N_H] d_H^T, \forall i \in \{1, \ldots, N\}.
\]

Note that the path-losses and the correlation matrices are assumed known after being obtained by practical methods, e.g., see [13]. Moreover, \(z_k \sim \mathcal{CN}(\bar{0}, \bar{1})\) describes the independent and identically distributed (i.i.d.) fast-fading vector in the \(k\)th link.

2) **Phase-shift errors:** The configuration of the RIS elements with infinite precision is not possible in practice. Hence, phase errors appear, which result from imperfections in phase-estimation and/or phase quantization that cannot be avoided [10]. Specifically, we denote \(\tilde{\phi}_n^k\), with \(n \in \mathcal{N}, k \in \{t, r\}\) the i.i.d. randomly distributed phase error in the \(n\)th phase-shift aiming at the \(k\)th UE. Hence, the random phase error matrix corresponding to the PBM \(\Phi_k\) is diagonal and described by \(\tilde{\Phi}_k = \text{diag}(e^{j \tilde{\phi}_1^k}, \ldots, e^{j \tilde{\phi}_N^k}) \in \mathbb{C}^{N \times N}\). The probability density function (PDF) of \(\tilde{\phi}_n^k\) is assumed symmetric with its mean direction equal to zero, i.e., \(\text{arg}(E[e^{j \tilde{\phi}_n^k}]) = 0\) [10].

In general, the Uniform and the Von Mises distributions are the main PDFs that can describe the phase noise affecting the RIS [10]. Notably, the Uniform PDF of phase-noise has a characteristic function (CF) equal to zero, and thus it cannot provide any knowledge regarding the phase-estimation accuracy. In contrast, the Von Mises PDF has a zero-mean and

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1In practical applications, the amplitude and phase-shifts are correlated and result in a performance loss. The study of this correlation is left for future work.

2This model can be easily extended to the multi-user scenario as in typical mmMIMO, where all UEs are divided into multiple groups of two UEs located at the opposite sides of RIS.

3The consideration of Rician fading, which includes an LoS component, is the topic of future work.
concentration parameter $\kappa_\omega$, which captures the accuracy of the estimation. In particular, the CF of the Von Mises noise CF is $m = \frac{w(\kappa_\omega \nu)}{d(\kappa_\omega \nu)}$, where $I_\nu(\kappa_\omega)$ is the modified Bessel function of the first kind and order $\nu$.

The received signal by UE $k \in \{t, r\}$ through the STAR-RIS assisted network is described by

$$y_k = \sqrt{\rho_{dl}} h_k^r \Phi_k^x X_k^x G_k^r f_k q_k + z_k,$$  \hspace{1cm} (5)

where $\rho_{dl} \geq 0$ is the transmit power at BS to UE $k$, and $q_k$ is the data symbol with $E[|q_k|^2] = 1$, while $f_k \in C^{M \times 1}$ is the linear precoding vector, and $z_k \sim CN(0, N_0)$ is the additive white Gaussian noise with zero mean and variance of $N_0$.

Notably, the cascaded channel vector including the phase-shift errors between the large BS and UE $k \in \{t, r\}$ can be expressed as $h_k = G_k^r \Phi_k^x h_k \in C^{M \times 1}$, where $X = ES, MS$. It is distributed as $CN(0, R_k)$, where $R_k = \beta_k G_k^r \Phi_{RIS}^x G_k^r$. Note that $R_{RIS} = E[\Phi_k^x \Phi_{RIS}^x \Phi_k^x] = m^2 R_{RIS} + (1 - m^2) I_N$, where $m$ denotes the CF of the phase error \[2 Eq. 13\]. In the case of the Uniform distribution, i.e., $m = 0$, $R_k$ does not depend on the phase-shifts and RIS cannot be optimized. A similar observation is met when RIS optimization is based on statistical CSI \[2\]. Hence, apart from its practical meaning, RIS correlation should be taken into account to exploit RIS.

III. MAIN RESULTS

This section presents the signal-to-noise ratio (SNR), the coverage probability, and its optimization for STAR-RIS assisted systems. Generally, the coverage probability for $k$th UE, $P_c^k$ with $k \in \{t, r\}$, is the probability that the received SNR is greater than a threshold $T$, i.e., it is described by $P_c^k = Pr(\gamma_k > T)$, where $Pr(\cdot)$ denotes probability.

A. SNR

First, we take advantage of channel hardening, because UEs do not have any knowledge of the instantaneous CSI in practice, but they are aware of their statistics \[15\]. Note that channel hardening appears in mMIMO systems as the number of BS antennas increases. Hence, by resorting to the application of the use-and-then-forget bounding technique \[15\], we write (6) as

$$y_k = \sqrt{\rho_{dl}} [E[h_k^r f_k] q_k + h_k^r f_k q_k - E[h_k^r f_k] q_k] + z_k.$$  \hspace{1cm} (6)

Next, by assuming that (6) represents a single-input single-output (SISO) system, where the BS treats the unknown terms as uncorrelated additive noise, the achievable SNR of the link between the BS and UE $k \in \{t, r\}$ is written as

$$\gamma_k = \frac{[E[h_k^r f_k] q_k + h_k^r f_k q_k - E[h_k^r f_k] q_k]^2}{E[|h_k^r f_k|^2]^2 + \sigma_0},$$  \hspace{1cm} (7)

where $\sigma_0 = N_0/\rho_{dl}$ \[15\]. Regarding the selection of precoding, we apply the simple maximum ratio transmission (MRT) precoding because it allows the derivation of closed-form expressions and extraction of fundamental properties together with its optimality for the single UE case, i.e., $f_k = \frac{h_k}{\sqrt{E[|h_k|^2]}}$.

**Proposition 1:** The downlink SNR of a STAR-RIS assisted mMIMO system with correlated Rayleigh fading and phase-shift errors at UE $k \in \{t, r\}$ is given by

$$\gamma_k = \frac{\text{tr}^2(R_k)}{\text{tr}(R_k^2) + \sigma_0 \text{tr}(R_k)},$$  \hspace{1cm} (8)

Another common choice could be the more robust regularized zero-forcing (RZF) precoder, but that could be applicable in a multi-user scenario with interference, and it would result in intractable expressions. Hence, the application of RZF could be the topic of future work.

**Proof:** See Appendix A.

**Remark 1:** As can be seen, the SNR in (8) depends only on the RZF and the statistical CSI by means of the correlation matrix, the path-losses, and the phase-shift errors. Also, there is a dependence on the location of UE $k$, i.e., if it is found behind or in front of the RIS.

B. Coverage Probability

Having obtained the SNR, the following proposition provides the coverage probability.

**Proposition 2:** The coverage probability of a mMIMO STAR-RIS assisted system, accounting for RIS correlation and phase-shift errors of UE $k \in \{t, r\}$, is tightly approximated as

$$P_c^k \approx \sum_{n=1}^{L} \left(\frac{L}{n}\right)^{n+1} e^{-\frac{n}{\eta}},$$  \hspace{1cm} (9)

where $\eta = L(\bar{L})^{-\frac{1}{2}}$ with $L$ being an approximation parameter.

**Proof:** See Appendix B.

The coverage depends on the threshold, the number $L$ defining the tightness of the approximation, and of course, the downlink SNR with its involved parameters.

**Conventional RIS:** We assume a smart surface that consists of transmitting-only or reflective-only elements, each with $N/2$ elements with $N$ even for simplicity. Also, $\beta_n^t = 1$ or $\beta_n^r = 1, \forall n$, respectively. In Sec. IV we compare the performance of the STAR-RIS with the conventional RIS and illustrate the advantage of adopting STAR-RIS in wireless systems.

C. Passive beamforming matrix optimization

A STAR-RIS assisted system serves two regions simultaneously, where UEs $t$ and $r$ are found. We focus on the optimization of the total coverage probability given by $P_c^t + P_c^r$. Given the difficulty in simultaneous optimization of both $P_c^t$ and $P_c^r$, we rely on alternating optimization by optimizing first each of them with respect to its PBM while fixing the other in an iterative manner until reaching the convergence, i.e., we perform optimization of $P_c^t$ with respect to $\Phi_k^r$. Each optimization is achieved in terms of the projected gradient ascent until converging to a stationary point.

Hence, based on the common assumption of infinite-resolution phase-shifters, the maximization algorithm for $P_c^k$, $k \in \{t, r\}$ UE with respect to the PBM is formulated as

$$\begin{align}
&P_k \max_{\Phi_k} P_c^k \\
&s.t. \beta_n^r + \beta_n^t = 1, \forall n \in N
\end{align}$$  \hspace{1cm} (10)

By replacing $[0, 1]$ with $\{0, 1\}$, (10) can be applied to the MS scheme.

The optimization problem (10) is non-convex regarding $\Phi_k^r$. The dependence on $\phi_n^r$ is found on the covariance matrices $R_k$. Given that it is a constrained maximization problem, we resort to the projected gradient ascent (PGA) until convergence to a stationary point to provide its solution \[2\]. The transmit power constraint guarantees its convergence. It is worthwhile to mention that the complexity of $P_c^k$ is $O(G(M^2 N^2 + M^3 + L))$. As can be seen, it is a function of the fundamental system parameters $M$, $N$, and $L$ with the number of BS antennas having the higher impact. Since it has to be performed twice for each $k \in \{t, r\}$, the complexity is double, while, in the case of the conventional RIS scenario, the complexity is half of the STAR-RIS setting.

Based on PGA, let $s_k \in \{\phi_n^r, \ldots, \phi_N^r\}^T$ denote the vector including the phases at step $l$, while the next iteration point provides the increase of $P_c^k$ upon its convergence by projecting
the solution onto the closest feasible point as specified by 
\[
\min_{\phi_k \in [0, 2\pi)} \|s_k - s_k^*\|^2.
\]
where the step size is determined by 
\[
\hat{s}_{k,t+1} = s_{k,t} + \mu \mathbf{v}_{k,t}.
\]
where the parameter \(\mu\) is the step size obtained at each iteration through the backtracking line search [16]. Moreover, \(\mathbf{v}_{k,t}\) is the ascent direction at step \(t\), which means 
\[
\mathbf{v}_{k,t} = \frac{\partial L_{\text{ANG}}}{\partial S_k}.
\]
where the following lemma provides this derivative.

Lemma 1: The derivative of the coverage probability for UE \(k \in \{t, r\}\) with respect to \(s_{k,t}\) is given by (17) at the top of the next page, where \(\gamma_k\) is given by (8), and
\[
S_k = \text{tr}^2 \mathbf{R}_k,
\]
\[
I_k = \text{tr} \mathbf{R}_k^2 + \sigma_0 \text{tr} \mathbf{R}_k,
\]
\[
\frac{\partial S_k}{\partial s_{k,t}} = 2\beta_k \text{tr} \mathbf{R}_k \text{diag}(G^\mathbf{w} \mathbf{G}^\mathbf{x}_k \bar{\mathbf{R}}^\mathbf{x}_{k,RIS}),
\]
\[
\frac{\partial I_k}{\partial s_{k,t}} = \beta_k \text{tr} \left( \mathbf{G}^\mathbf{w} \mathbf{R}_k \mathbf{G}^\mathbf{x}_k \bar{\mathbf{R}}^\mathbf{x}_{k,RIS} \right) + \frac{\sigma_0}{\beta_k} \text{tr} \left( \mathbf{G}^\mathbf{w} \mathbf{R}_k \mathbf{G}^\mathbf{x}_k \bar{\mathbf{R}}^\mathbf{x}_{k,RIS} \right).
\]

Proof: See Appendix C.

IV. NUMERICAL RESULTS

In this section, we provide the numerical results for the coverage of the STAR-RIS assisted mMIMO system. We consider a uniform planar array (UPA) of \(N = 60\) elements for the RIS, while a uniform linear array (ULA) with \(M = 40\) antennas is assumed for the BS that serves UEs \(t\) and \(r\). Unless otherwise stated, we consider the following values. The pathlosses are generated according to the NLOS version of the 3GPP Urban Micro (UMi) scenario from TR36.814 for a carrier frequency of 2.5 GHz, and noise level \(-80\ dBm\). Specifically, we have
\[
\beta_0 = C_d \gamma_0 \nu_v \quad \text{and} \quad \beta_k = C_d \gamma_k \nu_v, \quad k \in \{t, r\}
\]
\[
C_d = 26 \text{ dB}, \quad C_t = 26 \text{ dB}, \quad C_r = 28 \text{ dB}, \quad \nu_v = 2.1, \quad \nu_v = 2.2.
\]
where \(\gamma_k\) is the distance between the BS and RIS and between the RIS and UE \(k \in \{t, r\}\), respectively. We assume that the correlation matrix for the RIS is given by (8), where the horizontal and vertical dimension of each element is \(\alpha = 0.7\) and \(\nu = 0.7\). Also, we assume that \(\beta_k = 0.4, \beta_t = 0.6, \gamma_0 = 6 \text{ dB}, \text{ and } N_0 = -174 + 10 \log_{10} B_t, \text{ with } B_t = 200 \text{ KHz}.\)

Monte-Carlo (MC) simulations are carried out to verify our analysis.

In Fig. 2, we depict the coverage probability versus the target rate for varying number of RIS elements \(N\) while studying other key properties. We observe that a higher number of \(N\), increases \(P_c^k\) as expected. Moreover, we study the impact of phase errors for \(N = 25\), and we see that, in the case of Uniform PDF, where no knowledge on the errors is known, the RIS cannot be expected.

Moreover, we notice that independent Rayleigh fading conditions result in the worst coverage because no RIS exploitation can be achieved in the case of statistical CSI. In this direction, we observe that correlation should be taken into account to benefit from the RIS, while a higher correlation leads to lower coverage. For the sake of comparison, in the same figure, we have included the coverage in the case of a conventional RIS as presented in Sec. III-B with \(N = 30\) elements. Notably, the STAR-RIS system outperforms the conventional RIS-assisted system because more degrees of freedom for transmission and reflection can be harnessed.

V. CONCLUSION

In this paper, we obtained the coverage probability of a STAR-RIS assisted mMIMO system under the realistic assumptions of correlated Rayleigh fading and phase-shift errors, while previous works on STAR-RIS did not account for these inevitable effects. Especially, we derived the coverage probability for both \(t\) and \(r\) UEs in terms of large-scale statistics that change at every several coherence intervals, and thus, reduce the increased overhead of STAR-RIS. Among others, we depicted how the fundamental parameters affect the coverage, and the outperformance of STAR-RIS compared to reflective-only RIS. Future works could consider Ricean channels or even millimetre-wave transmission.
we define 

\[
\frac{\partial P_k}{\partial S_{k,l}} = \frac{\partial S_k}{\partial S_{k,l}} I_k - S_k \frac{\partial I_k}{\partial S_{k,l}} \gamma_k^2 n_{\frac{n+1}{2}} \sum_{n=1}^{L} \binom{L}{n} (-1)^{n+1} n \eta T e^{-\eta \frac{T}{\tau_k}}.
\] (17)

For the derivation of the second derivative in (24), i.e., \( \frac{\partial \gamma_k}{\partial S_{k,l}} \), we define \( \gamma_k = \frac{S_k}{\tau_k} \), where \( S_k = \text{tr}^2(\bar{R}_k) \) and \( I_k = \text{tr}(\bar{R}_k^2) + \sigma_0 \text{tr}(R_k) \). Hence, the derivative can be written as

\[
\frac{\partial \gamma_k}{\partial S_{k,l}} = \frac{\partial S_k}{\partial S_{k,l}} I_k - S_k \frac{\partial I_k}{\partial S_{k,l}} \gamma_k^2 \text{tr}(R_k^2), \quad (26)
\]

The computation of \( \frac{\partial S_k}{\partial S_{k,l}} \) follows. In particular, we have

\[
\frac{\partial S_k}{\partial S_{k,l}} = 2 \text{tr}(R_k) \text{tr}(R_k^l), \quad (27)
\]

where \( (\cdot)' \) denotes the partial derivative with respect to \( s_{k,l}^k \). Based on the property \( \text{tr} \left( A \text{diag}(s_{k,l}^k) \right) = (\text{diag}(A))^\top s_{k,l}^k \), where \( A \) is a matrix independent of \( s_{k,l}^k \), we can easily show

\[
\text{tr}(R_k) = \beta_k \text{diag}(G^\top G \Phi_k \bar{X}_k) \text{tr}(R_k). \quad (28)
\]

Regarding \( \frac{\partial I_k}{\partial S_{k,l}} \), we obtain

\[
\frac{\partial I_k}{\partial S_{k,l}} = 2 \text{tr}(R_k^l R_k^\top) + \sigma_0 \text{tr}(R_k^2). \quad (29)
\]

The derivative in (16) is obtained by (29) after exploiting the property used in (28). Substitution of the derivatives in (26) concludes the proof.

**REFERENCES**

[1] M. Di Renzo et al., “Smart radio environments empowered by reconﬁgurable intelligent surfaces: How it works, state of research, and the road ahead,” vol. 38, no. 11, pp. 2450–2525.

[2] A. Papazafeiropoulos et al., “Intelligent reﬂecting surface-assisted MIMO-MISO systems with imperfect hardware: Channel estimation, beamforming design,” IEEE Trans. Wireless Commun., 2021.

[3] C. Huang et al., “Reconﬁgurable intelligent surfaces for energy eﬃciency in wireless communication,” IEEE Trans. Wireless Commun., no. 8, pp. 4157–4170, 2019.

[4] C. Guo et al., “Outage probability analysis and minimization in intelligent reﬂecting surface-assisted MISO systems,” IEEE Commun. Lett., vol. 24, no. 7, pp. 1563–1567, 2020.

[5] A. Papazafeiropoulos et al., “Coverage probability of distributed IRS systems under spatially correlated channels,” IEEE Wireless Commun. Lett., vol. 10, no. 8, pp. 1722–1726, 2021.

[6] K. Zhi et al., “Statistical CSI-based design for reconﬁgurable intelligent surface-aided massive MIMO systems with direct links,” vol. 10, no. 5, pp. 1128–1132, 2021.

[7] Q. Wu and R. Zhang, “Intelligent reﬂecting surface enhanced wireless network via joint active and passive beamforming,” IEEE Trans. Wireless Commun., vol. 18, no. 11, pp. 5394–5409, 2019.

[8] E. Björnson and L. Sanguinetti, “Rayleigh fading modeling and channel hardening for reconﬁgurable intelligent surfaces,” IEEE Wireless Commun. Lett., vol. 10, no. 4, pp. 830–834, 2021.

[9] E. Papazafeiropoulos, “Ergodic capacity of IRS-assisted MIMO systems with correlation and practical phase-shift modeling,” IEEE Wireless Commun. Lett., vol. 11, no. 2, pp. 421–425, 2022.

[10] M.-A. Badiu and J. P. Coon, “Communication through a large reﬂecting surface with phase errors,” vol. 9, no. 2, pp. 184–188.

[11] J. Xu et al., “STAR-RISs: Simultaneous transmitting and reﬂecting reconﬁgurable intelligent surfaces,” IEEE Commun. Lett., vol. 25, no. 9, pp. 3134–3138, 2021.

[12] X. Mu et al., “Simultaneously transmitting and reﬂecting (STAR) RIS aided wireless communications,” IEEE Trans. Wireless Commun., 2021.

[13] F. Bohagen, P. Orten, and G. E. Oien, “Design of optimal high-rank line-of-sight MIMO channels,” IEEE Trans. Wireless Commun., vol. 6, no. 4, pp. 1420–1425, 2007.

[14] D. Neumann, M. Joham, and W. Utschick, “Covariance matrix estimation foundations and Trends® in Signal Processing,” IEEE Signal Process. Lett., vol. 22, no. 6, pp. 863–867, 2015.

[15] E. Björnson et al., “Massive MIMO networks: Spectral, energy, and hardware efficiency,” Foundations and Trends® in Signal Processing, vol. 11, no. 3–4, pp. 154–655, 2017.

[16] S. Boyd, S. P. Boyd, and L. Vandenberghe, Convex optimization. Cambridge university press, 2004.

[17] 3GPP. “Further advancements for E-UTRA physical layer aspects (Release 9),” 3GPP TS 36.814, Tech. Rep., 2017.

[18] T. Bai and R. W. Heath, “Coverage and rate analysis for millimeter-wave cellular networks,” IEEE Trans. on Wireless Commun., vol. 14, no. 2, pp. 1100–1114, 2015.