Coronal Electron Temperature Inferred from the Strahl Electrons in the Inner Heliosphere: Parker Solar Probe and Helios Observations

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Abstract

The shape of the electron velocity distribution function plays an important role in the dynamics of the solar wind acceleration. Electrons are normally modeled with three components, the core, the halo, and the strahl. We investigate how well the fast strahl electrons in the inner heliosphere preserve the information about the coronal electron temperature at their origin. We analyzed the data obtained by two missions, Helios, spanning the distances between 65 and 215 Rs, and Parker Solar Probe (PSP), reaching down to 35 Rs during its first two orbits around the Sun. The electron strahl was characterized with two parameters: pitch-angle width (PAW) and the strahl parallel temperature (T∥). PSP observations confirm the already reported dependence of strahl PAW on core parallel plasma beta (β∥). Most of the strahl measured by PSP appear narrow with PAW reaching down to 30°. The portion of the strahl velocity distribution function aligned with the magnetic field is for the measured energy range well described by a Maxwellian distribution function. T∥ was found to be anticorrelated with the solar wind velocity and independent of radial distance. These observations imply that T∥ carries the information about the coronal electron temperature. The obtained values are in agreement with coronal temperatures measured using spectroscopy, and the inferred solar wind source regions during the first orbit of PSP agree with the predictions using a PFSS model.

Unified Astronomy Thesaurus concepts: Solar wind (1534); Solar physics (1476); Space plasmas (1544); Space vehicle instruments (1548); Astronomy data analysis (1858); Solar corona (1483); Solar atmosphere (1477)

1. Introduction

The solar wind is the constant flux of plasma that leaves the solar corona and expands in our solar system (Parker 1958). It consists of mostly electrons and protons, both exhibiting nonthermal velocity distribution function (VDF) features. Electrons are usually modeled by three components. The lower electron energies are dominated by the core, Maxwellian-like population taking up most of the total electron density. Electrons with higher energies are either part of the magnetic field–aligned strahl population or of the halo population present at all pitch angles (Feldman et al. 1975; Pilipp et al. 1987; Maksimovic et al. 2005; Sverak et al. 2008; Sverak et al. 2009; Tao et al. 2016; Wilson et al. 2019a, 2019b; MacNeil et al. 2020). These models were based on the observations of the solar wind far from the Sun (the closest at 0.3 au), where the solar wind already propagates with a supersonic velocity and where most properties of the pristine coronal plasma have been changed. But how does the electron VDF look like in the solar corona? Does it exhibit high energy tails, or is the excess of the high-energy electrons observed in the interplanetary solar wind created during the expansion from purely Maxwellian coronal electrons?

Multicomponent distribution functions are used in the kinetic exospheric models of the solar wind initially assuming collisionless evaporation of the solar corona into interplanetary space (Jockers 1970; Lemaire & Scherer 1971). The acceleration of the solar wind in these models is provided by solar wind electrons. As their velocities are much higher than the velocities of protons with the same temperature in the solar corona, a portion of electrons manage to escape the Sun and create charge imbalance in the plasma. The imbalance gives rise to an anti-sunward-directed electric field, accelerating the heavier solar wind protons. This dynamics produces two main populations in electron VDF. Electrons with energies smaller than the electric potential energy needed to sustain the anti-sunward electric field are bounded to the Sun and present the dense thermal core population. The faster anti-sunward-directed electrons, which are able to overcome the potential, escape and form the strahl. The escaping strahl electrons are governed by the magnetic momentum ($\frac{m_e v^2}{2R} = \text{const.}$) and
energy ($E_{\text{kin}} + E_{\text{pot}} = \text{const.})$ conservation. As they expand into regions with a weaker magnetic field, they experience focusing (Schwartz & Marsch 1983).

Similarly, a two-component VDF was obtained by the exospheric models accounting for collisions with the Fokker–Planck equation solver using a test particle approach (Liev-Svendsen et al. 1997; Pierrard et al. 2001; Smith et al. 2012) and by the kinetic simulation of the solar wind accounting for Coulomb collisions statistically (Landi et al. 2012, 2014).

These models describe well the formation of the core and the strahl, but they do not explain the formation of the halo. It is possible that the halo is already present in the solar corona, consisting of hot electrons leaking from the dense coronal regions with closed magnetic field loops. Exospheric models assuming an excess of high-energy electrons in the corona were the first models able to self-consistently produce fast solar wind reaching velocities above $\sim 700 \text{ km s}^{-1}$ (Maksimovic et al. 1997a; Dorelli & Scudder 1999; Lamy et al. 2003; Zouganelis et al. 2004).

On the other hand, observations have shown that the relative density of the two high-energy electron populations exchanges as a function of radial distance. The strahl is more pronounced close to the Sun while the halo density increases over the radial distance (Štverák et al. 2009). This suggests that the halo is not present in the solar corona and is formed during the solar wind expansion from the strahl component.

The strahl and the halo populations, not sensitive to collisions, were early assumed to be the remnants of the hot coronal electrons in the solar wind (Feldman et al. 1975). The focusing mechanism experienced by the strahl during the expansion does not affect the shape of the magnetic field-aligned cut through the strahl VDF ($f_{\parallel}$) nor the strahl parallel temperature ($T_{\parallel}$). Therefore, the strahl, in the absence of collisions any other interactions, preserves the temperature and the shape of the VDF of the coronal electrons at its origin.

This is only valid in the kinetic models not including collisions or wave–particle interactions. The strahl electrons have been observed to not focus but scatter with radial distance (Hammond et al. 1996; Graham et al. 2017; Berčić et al. 2019) accounting for phenomena to some extent to Coulomb collisions (Horaites et al. 2018, 2019), but also to wave–particle interactions (Vocks et al. 2005; Kadić et al. 2016) and scattering by the background turbulence (Pagel et al. 2007; Saito & Gary 2007). Graham et al. (2017) report that the strahl was rarely observed at distances higher than 5 au. The strahl and the halo electrons do interact with the surrounding plasma and electric and magnetic fields but on much larger spatial scales than the thermal, core electron component.

The core electron temperature was recently found to be correlated to the solar wind origin in the inner heliosphere; however, the correlation is almost completely lost by the time the solar wind reaches the distance of 1 au (Maksimovic et al. 2020).

Whether the high-energy electron components preserve information about the solar wind origin at the radial distance of 1 au has been tested through comparison to the oxygen charge-state ratio ($O^{+\ast}/O^{+\ast}$), an established proxy for measuring the coronal electron temperature. While Hefti et al. (1999) find a correlation between the $T_{\parallel}$ and the oxygen charge-state ratio, MacNeil et al. (2017) find that the correlation is not very strong, and it varies depending on the choice of interval.

We aim to investigate whether the information about the solar wind origin is present at the closest distances sampled by in situ instruments so far: 35 $R_{\odot}$ for the Parker Solar Probe (PSP) and 65 $R_{\odot}$ for the Helios mission. As the oxygen charge-state ratio is not measured by these two space crafts, we use the solar wind velocity as an indicator of the solar wind origin.

2. Data Sets

2.1. Parker Solar Probe

Launched in 2018 August, PSP (Fox et al. 2016) is a mission designed to study the solar wind in the vicinity of the Sun, eventually reaching as close as 8.8 $R_{\odot}$ from its surface. We analyze the data gathered during the first two orbits of PSP with the perihelion of 34.7 $R_{\odot}$ and the aphelion between the orbits of Venus and Earth.

Electrons on board PSP are measured with two SPAN Electron (SPAN-E) electrostatic analyzers: SPAN-A and SPAN-B (Whittlesey et al. 2020), part of the SWEAP instrument suite (Kasper et al. 2016). Positioned on the ram and on the anti-ram side of the spacecraft with their 120° × 240° field of views (FOVs) 90° tilted with respect to each other, they cover almost a full 4π solid angle. The azimuth angle ($\phi$) on each of the SPAN-ES is measured by eight small (6°) and eight large (24°) anodes, while the elevation ($\theta$) angles are sampled by the electrostatic deflectors. During the first two encounters, deflectors separated the elevation measurements in eight angular bins with a resolution of 20°, of which the two extreme elevation bins have not been used in our analysis. The combined FOV of the two instruments is represented in Figure 1, where the gray surfaces represent solid angles that are not sampled by the instruments. To be able to withstand high levels of solar radiation, PSP is equipped with a heat shield. When the spacecraft is within 0.7 au from the Sun, the shield points straight to it and blocks approximately an angle of 10° from the Sun-spacecraft line (the center of the FOVs in Figure 1). Electron energy is measured by toroidal electrostatic analyzers, which are adapted to the high variation of electron fluxes with a mechanical attenuator controlling the size of the entrance to the aperture. Energies between 2 eV and 2 keV are sampled in 32 exponentially spaced bins with the energy resolution ($\Delta E/E$) of 0.07.

The duration of one sweep over all the energy and deflection bins is 0.218 s. The data product used for the presented data analysis are full 3D spectra (32 energies, 8 elevations, 16 azimuths) integrated over a period of 27.9 s during Encounter 1 (2018 October 29–November 14) and over a period of 14.0 s during Encounter 2 (2019 March 29–April 10). When the spacecraft is farther from the Sun (>60 $R_{\odot}$), the instruments are operating in cruise mode with the cadence of 895 s and integration period of 27.9 s.

Detailed descriptions of the SPAN-E instruments and their operating modes are provided by Whittlesey et al. (2020).

In addition to the electron measurements, we use the solar wind proton velocity and density moments calculated from the SPC instrument (Case et al. 2020) and a vector magnetic field measured by a triaxial fluxgate magnetometer MAG part of the FIELDS investigation (Bale et al. 2016). SPC is a Faraday cup instrument stuck out of the heat shield and measuring the plasma flowing directly from the Sun, also part of the SWEAP investigation (Kasper et al. 2016). The cadence of both, SPC and MAG, is higher than that of SPAN-E; thus, the averages...
over the duration of each full SPAN spectra are used in further analysis.

2.2. Helios 1

The predecessors of the PSP are the two Helios missions launched in the 70 s (Porsche 1981). For more than 6 years, these two spacecraft were exploring the inner heliosphere down to 0.3 au (64 R$_S$) and providing us with a big data set of various solar wind parameters, among others revealing radial and solar cycle related trends (Feldman et al. 1975; Pilipp et al. 1987; Maksimovic et al. 2005; Marsch 2006; Šverák et al. 2009). These data were of great importance during the preparation for the PSP mission and stay important due to the large statistics and radial and time coverage. In this work, we use the data from Helios 1 gathered between 1974 and 1980.

Electron VDFs on board the Helios 1 mission are sampled by a single narrow $2^\circ \times 19^\circ$ FOV aperture, which uses spacecraft spin to obtain a 2D measurement in the plane perpendicular to the spin axis. The sampled plane is aligned with the ecliptic plane. The $360^\circ$ azimuth angle measurement is completed in 8 steps resulting in $28^\circ$ wide azimuth bins with gaps in between them (see schematics in Figure 4(a)). Energies between 9 eV and 1.5 keV are sampled in 16 exponentially spaced energy steps. The full 2D measurement (16 energies, 8 azimuths) is completed in 16 s with a cadence of 40 s.

The proton onboard integrated densities and velocity vectors were taken from the original Helios files in Helios data archive.14

The magnetic field vector is a composite measurement of two fluxgate magnetometers: E2 for all instances where measured magnetic field was less than 50 nT, and E3 for the rest. More details about the Helios data set and instrumentation can be found in our previous work with Helios observations (Berčič et al. 2019).

3. Method

3.1. Parker Solar Probe

The measured electron distribution functions are subject to instrumental as well as environmental effects. An important issue on the instrumental side is the determination of the sensitivities of each of the azimuth anodes. The sensitivity coefficients used for our analysis were obtained through in-flight calibration described in the work of Halekas et al. (2020). The effects of the spacecraft own magnetic field and electric charge on the particle trajectories were studied by McGinnis et al. (2019). They show that, even though the spacecraft magnetic field is relatively large (it was predicted to reach the strength of 500 nT), the effect on some of the plasma moments is small (see Table 2 in McGinnis et al. 2019). The biggest errors were found for the bulk velocity calculation, as it strongly depends on low-energy measurements. The smallest errors, on the other hand, arise for the temperature calculation, as it is more dependent on higher-energy measurements. The spacecraft potential was estimated to be low, on the order of a few Volts negative during the flight calibration described, as it is more dependent on higher-energy measurements. Here we believe that our results are not affected significantly by these effects, which are more relevant for the low-energy electrons (Salem et al. 2001).

The instruments’ lower-energy bins are contaminated by secondary electrons emitted from the spacecraft. Halekas et al. (2020) choose to include them in their fitting model as a Maxwellian distribution with a temperature of 3.5 eV. For the

14 Link to the data archive: http://helios-data.ssl.berkeley.edu.
are detected by SPAN-A agreeing with the FOV representation in Figure 1. The strahl electrons in this scan measured by SPAN-E instruments on November 5 at 9:25:18 same on both sides of the plot, as there is no preferred direction perpendicular and directed in the anti-sunward direction. The perpendicular values are the common RTN velocity vectors from their initial instrument frame to the spacecraft from the Sun. The magnetic field direction lies within the dark blue area of the FOV covered by the small anodes of the SPAN-A, and the strahl VDF. An opposite case, when the strahl is the strahl electrons are measured with the angular resolution of 604 eV—part of the strahl VDF. An opposite case, when the strahl is this happens is shown on the right side of Figure 1. At lower energies where the width of the strahl electron beam is larger (upper FOV: 253 eV), the effect of the FOV obstruction does not play a big role, while at high electron energies (lower FOV: 604 eV) where the strahl electron population often appears very narrow, we might be missing a big part of the strahl VDF. An opposite case, when the strahl is detected as accurately as possible, is presented on the left side of Figure 1. When the magnetic field direction lies within the area of the FOV covered by the small anodes of the SPAN-A, the strahl electrons are measured with the angular resolution of 6 × 20° (azimuth × elevation) (Whittlesey et al. 2020). We do not wish to limit our data set with respect to the magnetic field

\[ f_c(v_{1,2}) = A_c \exp \left( \frac{(v_{1,2} - \Delta v_{1,2})^2}{w_{1,2}^2} \right) \]

where \( \Delta v_{1,2} \) are the drift velocities corresponding to three axes of the magnetic field–aligned frame. The fits were performed on the full three-dimensional VDFs using a least-square minimization algorithm\(^{15}\) provided by Scipy Optimization package for Python programming language (Virtanen et al. 2019). Because the VDF values span over several orders of magnitude (see Figure 2), the fitting was carried out in logarithmic space (\( \ln(f_c) \)). This technique decreases the large difference in the weight of fitted data points, giving more importance to the low VDF values. From our six fitting parameters—\( A_c, w_{1,2}, w_\perp, \Delta v_{1,2} \)—we can obtain the core density \( n_c \) from:

\[ n_c = A_c \cdot \pi^{\frac{3}{2}} w_\perp^2 w_{1,2}^2 \]  \( (2) \)

The thermal speeds parallel (\( w_{\parallel} \)) and perpendicular (\( w_{\perp} \)) to the magnetic field can be expressed in terms of core temperature \( T_{\perp,\parallel} \):

\[ T_{\perp,\parallel} = \frac{m_e w_{\perp,\parallel}^2}{2k_B} \]  \( (3) \)

where \( k_B \) is the Boltzmann constant and \( m_e \) is the mass of an electron. The core density and parallel temperature are then used to calculate the electron parallel plasma beta parameter:

\[ \beta_{\parallel} = \frac{2\mu_0 n_c k_B T_{\parallel}}{B^2} \]  \( (4) \)

with \( \mu_0 \) standing for vacuum permeability and \( B \) for magnetic field.

An example of electron VDF measured on the November 5 is presented with the cuts through the parallel (\( \parallel \)) and the perpendicular (\( \perp \)) direction with respect to the magnetic field in Figure 2. We recognize the expected electron VDF features: a core fitted with a bi-Maxwellian distribution (dashed line in the Figure 2), a field–aligned strahl component only seen parallel to the magnetic field direction, and a weak halo departing from a Maxwellian fit at higher electron energies. Another feature we do not plan to discuss in the present work, already observed by Halekas et al. (2020), can be recognized in Figure 2. Directed toward the Sun (on the left side) and aligned with the magnetic field (dark blue), there appears to be a deficit in the core electron distribution—a part of phase space where the measured VDF appears to be smaller than the best-fitting Maxwellian distribution function.

Even though the two SPAN-E instruments cover almost a full solid angle, there exist cases when the electron VDFs are not fully characterized by the measurement. As introduced in Section 1, we investigate the behavior of the strahl electrons, a population aligned with the magnetic field and directed away from the Sun. The magnetic field closer to the Sun fluctuates around a vector more and is more aligned with the radial direction following the Parker spiral model (Parker 1958). This means that, often, the magnetic field measurement over one full SPAN-E scan duration will lie in the portion of the FOV where the solar wind electrons are blocked by the spacecraft heat shield (marked with gray in the center of the FOVs in Figure 1). A case when this happens is shown on the right side of Figure 1. At lower energies where the width of the strahl electron beam is larger (upper FOV: 253 eV), the effect of the FOV obstruction does not play a big role, while at high electron energies (lower FOV: 604 eV) where the strahl electron population often appears very narrow, we might be missing a big part of the strahl VDF. An opposite case, when the strahl is detected as accurately as possible, is presented on the left side of Figure 1. When the magnetic field direction lies within the area of the FOV covered by the small anodes of the SPAN-A, the strahl electrons are measured with the angular resolution of 6 × 20° (azimuth × elevation) (Whittlesey et al. 2020). We do not wish to limit our data set with respect to the magnetic field

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\(^{15}\) scipy.optimize.leastsq (https://docs.scipy.org/doc/scipy/reference/generated/scipy.optimize.leastsq.html).
direction because we expect that the physical mechanisms shaping the electron VDFs will also depend on the magnetic field vector. Instead, we use a fitting method described below that accounts for the field-of-view limitation. The differences resulting from the FOV obstruction are further analyzed and presented in Appendix A.

We characterize the strahl electrons with two parameters: strahl pitch-angle width (PAW) and strahl parallel temperature ($T_{\|}$).

We expect to observe the strahl component aligned with the magnetic field and moving away from the Sun. This means that if the magnetic field radial component is negative, the strahl electrons will be antiparallel to the magnetic field vector. However, this is not always the case. Bi-directional strahls have been observed and related to magnetic field structures like closed magnetic loops and magnetic clouds (Gosling et al. 1987). Sunward-directed strahls have also been observed and serve as the indicators of magnetic field structures sometimes referred to as the switchbacks (Pilipp et al. 1987; Balogh et al. 1999; Yamauchi et al. 2004; MacNeil et al. 2020), which are frequently observed also during the first perihelion of the PSP (Bale et al. 2019; Kasper et al. 2019). In this study, we do not consider special cases and focus on the anti-sunward moving strahl electrons in the nominal solar wind.

To obtain the strahl PAW, we first calculate pitch angles ($\alpha_i$) for each measured energy bin of the electron VDF put in the plasma rest (defined by the solar wind protons) and magnetic field–aligned frame using the following criteria:

\[
\text{if } B_r > 0: \quad \alpha_i = \arccos \left( \frac{v_i}{\sqrt{v_i^2 + v_{\perp}^2}} \right),
\]

\[
\text{if } B_r < 0: \quad \alpha_i = \arccos \left( \frac{-v_i}{\sqrt{v_i^2 + v_{\perp}^2}} \right),
\]

The obtained pitch angles ($\alpha_i$) thus lay on the interval $[0^\circ, 180^\circ]$, where $0^\circ$ denotes the direction along the magnetic field and pointing away from the Sun, $90^\circ$ direction perpendicular to the magnetic field, and $180^\circ$ the direction along the magnetic field and pointing toward the Sun.

These pitch-angle distributions are then fitted for each energy bin separately with a Gaussian distribution function:

\[
f_i(\alpha) = f_{\text{max},i} \cdot \exp\left( -\frac{\alpha_i^2}{2\sigma_i^2} \right),
\]

where subscript $i$ denotes iteration over all of the energy bins. Two fits are preformed for each energy bin. A first fit to all of the available points in an energy bin to separate the strahl from the background, and a second fit only to the points aligning with the first fit selected by the following criteria:

\[
|f_{\text{data}} - f_{\text{fit},i}|/f_{\text{data}} < 0.99,
\]

where $f_{\text{data}}$ are the data points and $f_{\text{fit},i}$ are the values predicted by the first fit. The second fit was performed when at least four data points conform to the criteria above (Equation (8)). Two examples of the second fit are shown in Figure 3(a) (dashed lines). The selected points representing the strahl part of the distribution are marked with red or blue color. We use the parameters from the second fit to then calculate the FWHM, which we refer to as the PAW:

\[
\text{PAW}_i = 2\sqrt{\ln 2} \cdot \sigma_i,
\]

The instances when PAW exceeds the value of $180^\circ$ are excluded from further analysis, as they indicate almost
isotropic pitch-angle distributions and could be dominated by one of the more isotropic solar wind electron components, the core or the halo. In this work, we choose to perform the PAW analysis on the full electron VDF and not only on the strahl VDF, which can be obtained by subtraction of the modeled core and halo components from the total measured VDF (as done by Berčič et al. 2019, Section 3.2). Using the full VDF, we avoid the errors resulting from the core and the halo modeling. The core population taking up the lower electron energy is more sensitive to the effects of spacecraft’s magnetic and electric fields and exhibits the yet unstudied deficit in the sunward, magnetic field–aligned portion of the VDF. The halo component is difficult to model because it was observed to be very tenuous and, during the encounter periods when the instrumental mechanic attenuator was closed, represented only by a few data points (Halekas et al. 2020). The strahl component, on the other hand, takes up higher energies and appears relatively dense, especially during the encounter periods. For these reasons, we fit Equation (7), the full measured VDF, and rely on the assumption that the energy bins resulting in PAW $<180^\circ$ are dominated by the strahl electron component. The same approach was used by Hammond et al. (1996) and Graham et al. (2017). An example of the PAWs calculated for each energy bin of one measured scan is shown in Figure 3(b).

In the inner heliosphere and for the energy ranges sampled by the SPAN-E instruments, the strahl VDFs along the parallel direction to the magnetic field are well represented by a Maxwellian distribution function. For the scope of this work, we are only interested in the temperature of this Maxwellian—the slope of the parallel strahl VDF. However, the peak of the pitch-angle distributions aligned with magnetic field is sometimes not sampled due to the heat shield FOV obstruction. Thus, instead of using the measured VDF closest to the parallel direction, we use the maximum VDF values ($f_{\text{max}}$) from the fit to the pitch-angle distributions at each energy bin (see Equation (7)).

We perform a fit in the parameter space where a Maxwellian distribution forms a straight line with a slope depending only on its temperature:

$$\ln f_{\text{max},s}(v_s) = -\frac{m_e}{2k_B \cdot T_s} \cdot v_s^2 + \ln \left( \sqrt{\frac{m_e}{2\pi k_B \cdot T_s}} \right).$$

(10)

where ln denotes the natural logarithm. An example of the strahl distribution in this representation is shown in Figure 3(c). Fitting a straight line in this parameter space, we assume that the drift velocity of the Maxwellian is zero or very small in comparison to the electron velocity ($v$). This agrees with the exospheric models predicting that the VDF stays the same as in the corona, where the bulk velocity of electrons is zero.

3.2. Helios 1

The same two parameters to characterize the strahl electrons, PAW and $T_s$, were obtained from the Helios 1 observations. The PAWs as well as some other parameters like the core electron density ($n_c$) and temperature ($T_{c\parallel}$), velocity of the protons ($v_p$), and magnetic field ($B$), have already been used and are described in our previous work (Berčič et al. 2019).

The strahl temperature is determined in a similar way as described for the PSP; however, the Helios 1 mission did not have a heat shield, and the 2D electron instrument was able to point straight at the Sun. Thus, using the $f_{\text{max},s}$ parameter from the PAW fits is not necessary. Instead, we limit the data set to instances when magnetic field lies within one of the eight azimuth bins and fit the Equation (10) to the data points from this azimuth bin (marked in blue in Figure 4(a)). We use a full measured distribution function in this bin and not the strahl distribution presented in Berčič et al. (2019), which was obtained by subtraction of the core and the halo from the measured VDF ($f_{\text{strahl}} = f_{\text{measured}} - f_{\text{core}} - f_{\text{halo}}$). The full distribution was used to unify the methods of $T_s$ calculation between PSP and Helios data set.

This process is illustrated in Figure 4(b). From the Helios data set, it is not as obvious that the strahl parallel VDF can be modeled by a Maxwellian. The VDFs appear noisier, and especially farther from the Sun (lighter blue values Figure 4(b)), they may exhibit traces of high energy tails, previously modeled by Kappa-like distribution functions (Maksimovic et al. 1997a; Štverák et al. 2009). However, for a certain energy range (between $\sim200$ and $800$ eV), strahl VDFs still present a straight line in the $\ln(f(v^2))$ parameter space and give us the information about the strahl parallel temperatures. Fitting only the selected energy range, we avoid the inclusion of the electron core component.

4. Observations

Strahl PAWs with respect to electron energy for the different plasma $\beta_{\text{ec}}$ values are shown in Figure 5. Only data gathered during the first two encounter periods (35–60 Rs) was used and plotted separately ((a)—encounter 1, (b)—encounter 2). We separated the data because of the different integration time of the instruments for each encounter (see Section 2.1) and because of an unresolved issue with the instruments’ response during the encounter 2. This artifact can be seen in Figures 5(b), A1(b), and B1(b) as a zig-zag pattern of PAW along the energy dimension for higher energies. It appears as if the PAW is slightly broader for every second energy bin. A possible reason for this kind of measurement response could lie in the hysteresis of the instrument deflection plates. A predicted correction for this effect has been applied on the whole data set; however, the hysteresis could be time dependent with a stronger effect on the measurements made during encounter 2. Nevertheless, the irregularities do not exceed the statistical error and, thus, do not change any conclusions of the present work.

Both plots in Figure 5 show the increase of PAW with $\beta_{\text{ec}}$. For the lower two $\beta_{\text{ec}}$ cases, the PAW decreases with electron energy reaching down to 30eV, while for the highest $\beta_{\text{ec}}$ case the PAW stays more or less constant with a value $\sim55eV$ for the energies above $\sim200eV$. This high-$\beta_{\text{ec}}$ regime where the strahl appears to be more affected by the scattering mechanisms was found for 26% of electron spectra during the encounter 1 and for 13% during encounter 2. For all cases, a fast increase of PAW is observed for the low electron energies, denoting the presence of the electron core population below the energy of $\sim200eV$.

No radial dependence was found during the encounter periods (from 35 to 60 Rs), most likely as a consequence of the presently limited PSP data set. It appears that the type of the
solar wind we observe has more of an effect on PAW than the radial distance.

Strahl temperatures obtained from Helios and PSP data sets are presented separately in Figures 6 and 7. The results from Helios data set are the outcome of binning several years’ of solar wind measurements, while for the PSP, we use the data obtained over less than 6 months. Nonetheless, during the PSP encounter periods, the data rate is very high, and we were lucky to have already sampled different types of solar wind providing us with a satisfactory statistics. For the Helios data set, sampled distances range from 65 to 215 $R_S$, while for that of the PSP, the radial coverage is much smaller, from 35 and 58 $R_S$ (first two encounters). Similarly, measured proton velocities in the PSP data set have a smaller span than in the Helios data set.

The 2D histograms in both cases show the same result, no strong trends in variation of the $T_{SP}$ with radial distance ($r$) and an anticorrelation with the solar wind proton velocity ($v_p$). The overall mean value of $T_{SP}$ measured by PSP is 93 eV with a standard deviation of 13 eV, and by Helios 105 eV with a standard deviation of 23 eV.

Figure 8 presents the evolution of $T_{SP}$ with part of the PSP orbit 1 trajectory ballistically projected down to the corona ($2 R_S$) to produce sub-spacecraft points (marked with colored dots). SWEAP in situ proton velocity measurements are used to perform this projection. The colored lines show the magnetic field lines mapped from each of the sub-spacecraft points down to the solar surface as predicted by the PFSS model (see Bale et al. 2019; Badman et al. 2020 for more details about the PFSS modeling). The polarity inversion line is shown in white.

This interval was chosen because it exhibits distinctive coronal features: a small coronal hole occurring during the first encounter period (region marked with a box in upper plot in Figure 8, enlarged in the lower plot), and a big coronal hole occurring after the encounter period (the center of the upper
plot in Figure 8). Coronal holes appear as the darker parts in the images produced from the 193 Å emission line, as these are the regions marked by low plasma density and open magnetic field lines. Oppositely, the bright regions in the image correspond to higher plasma densities, normally related to closed magnetic field loops. A similar plot has been shown in the work of Badman et al. (2020), who use a PFSS model to map the magnetic field lines measured by the spacecraft back to the solar surface (see Figures 5 and 8 in the referred article).

Our crude separation of $T_{s\|}$ appears to discern distinct coronal features as identified in the PFSS model: Very low $T_{s\|}$ (marked in black in Figure 8) is measured as $PSP$ traces over the larger, positive polarity coronal hole after the first encounter and measured a fast wind stream, while a mix of intermediate $T_{s\|}$ (blue) and high $T_{s\|}$ (red) occurs in association with the smaller coronal hole $PSP$ looped over at perihelion. The high strahl temperatures are associated with mapping to the edges of the coronal hole and the proximity to the current sheet (white contour in Figure 8), while the intermediate temperature occurs at a time when the solar wind bulk speed increased and $PSP$ was directly over the center of the coronal hole.

In lower plot in Figure 8, presenting a zoom-in of the first encounter, the intermediate $T_{s\|}$ do not correspond directly to the darker regions on the image. Coronal holes are dynamic features, and this small coronal hole has been observed to drift over the limb of the Sun on November 2 (a date marked in

Figure 6. Histograms showing the variation of $T_{s\|}$ with radial distance ($r$) (left panel), and solar wind proton velocity ($v_p$) (right panel) for the Helios data set. The histograms are normalized to the maximum value in each vertical column. Above each of the 2D histograms and on the right side, 1D histograms present the probability distribution of the corresponding parameters ($r$, $v_p$, and $T_{s\|}$).

Figure 7. Histograms showing the variation of $T_{s\|}$ with radial distance ($r$) (left panel), and solar wind proton velocity ($v_p$) (right panel) for the $PSP$ data set. The histograms are normalized to the maximum value in each vertical column.
Therefore, we cannot be sure of the position of the small coronal hole at the time of the PSP crossing, and a slight disagreement between the image and $T_{SP}$ is expected.

### 5. Discussion

PAWs observed by the PSP agree very well with the reported observations from the Helios mission (Figure 4 in Berčič et al., 2019). The most obvious change in the radial evolution from the closest regions to the Sun probed by Helios spacecraft ($65 R_S$) to the first two perihelia of the PSP reaching down to $35 R_S$ is the fast increase in PAW at low electron energies (see Figure 5). We attribute this increase to the presence of the core electron component reaching the temperatures above $30\,\text{eV}$ (Halekas et al., 2020).

The observed anticorrelation between PAW and electron energy for the lower two $\beta_{ec}$ bins (Figure 5) might be a consequence of a collisionless focusing mechanism. Focusing of the solar wind electrons starts taking place at a distance above the solar surface where collisions cannot dominate the electron VDF anymore, a distance in the frame of exospheric solar wind models referred to as the exobase (Jockers 1970; Lemaire & Scherer 1971). The location of the exobase can be between 2 and $10\,R_S$ (Maksimovic et al. 1997a) and depends
on the type of the solar wind. The expected relation between PAW and electron energy at the distance of 35 \( R_S \) accounting only for the focusing mechanism is shown in Figure 9 for the low and the high exobase limit. The model assumes an isotropic Maxwellian VDF at the exobase expanding along a radially decreasing magnetic field (\( B \propto 1/r^2 \)). Following energy and momentum conservation (Equation (6) in Berčić et al. 2019), we obtain a VDF at 35 \( R_S \) and calculate the PAW as described in Section 3. In comparison to the majority of observations, the modeled PAWs still appear at least two times narrower.

In reality, the transition between collision-dominated and collisionless regimes does not happen at one distance but is a continuous process. This could be one of the reasons why our single exobase focusing model predicts lower PAWs than observed. Another possibility is that the strahl has already been affected by scattering mechanisms also resulting in an anticorrelation between PAW and electron energy. A good candidate is Coulomb collisions. A study using kinetic theory is presented in works by Horaites et al. (2018, 2019), providing a theoretical prediction of the strahl PAW, accounting for collisions between particles. PAW seems, to some extent and for some energy range, to agree with the results from Horaites et al. (2018), predicting relations in the form \( \text{PAW} \propto \sqrt{n} \), and \( \text{PAW} \propto E^{-1} \), where \( n \) strands for density and \( E \) for electron energy. However, Equation (15) from Horaites et al. (2019) does not predict our observations.

The focusing experienced by the strahl electron component during the solar wind expansion does not affect \( T_{\|} \). If the scattering mechanisms do not strongly modify the electron VDF, the temperature of the VDF at the exobase stays imprinted in the strahl population. The density of the VDFs and the core \( T \) decrease with radial distance, but the slope—the temperature—of the parallel cut through the strahl part of the VDF remains unchanged (see schematics in Figure 10). Even though the strahl PAW are observed to be somewhat broader than that predicted by the exospheric models, no radial trends were found in the \( T_{\|} \) observed by Helios and PSP missions (see Figures 6 and 7). This raises the question of the efficiency of the scattering mechanisms in modifying \( T_{\|} \). The answer requires further observational and numerical studies, which are beyond the scope of this work.

The constant behavior of \( T_{\|} \) over radial distance is a new observation, which is in contradiction with the current beliefs about its radial evolution. Recent near-Earth observational studies, from either Wind or Cluster spacecraft (Viñas et al. 2010; Tao et al. 2016; MacNeil et al. 2017; Wilson et al. 2019b), report significantly lower strahl \( T \) than the ones reported in this work. As a consequence, it was accepted that the strahl temperature must decrease over the distance from Sun to Earth. But the reason for different observational results lies mostly in the different data analysis approach. We follow the exospheric theory and, therefore, fit the strahl field-aligned VDF cut with a Maxwellian centered on \( v_\| = 0 \). Viñas et al. (2010) isolate the strahl component and obtain the plasma moments by integration. The obtained strahl \( T \) are on the order of 10 eV with \( T_\perp \sim 2 \) times bigger than \( T_{\|} \), and the obtained drift velocities are relatively high. With this approach, they measure the width of the strahl distribution, while we are interested in the slope. Wilson et al. (2019b) model the strahl with a Kappa distribution with a drift and report the mean \( T_{\|,K} \) of 44.2 eV. Tao et al. (2016) and MacNeil et al. (2017) also use Kappa distribution function but centered on \( v_\| = 0 \), and they find means \( T_{\|,K} \) of 51.1 eV and \( ~50 \) eV, respectively. We performed a test to quantify the effect of the different model choice on the obtained \( T_{\|} \). Figure 11 shows the same example as Figure 3(c) but fitted with a Kappa distribution function for \( \kappa = 10 \) and \( \kappa = 5 \). The fit was made in the logarithmic space with the one-dimensional Kappa distribution function:

\[
 f_\kappa (v_\|) = \frac{n_\kappa}{\kappa^{3/2} \sqrt{\pi} w_\kappa} \frac{\Gamma(\kappa + 1)}{\Gamma(\kappa - 1/2)} \left[ 1 + \frac{v_\|^2}{w_\kappa^2} \right]^{-\kappa - 1}, \tag{11}
\]

where the \( \kappa \) parameter is given, and the density (\( n_\kappa \)) and the thermal velocity (\( w_\kappa \)) are the fitting parameters. The strahl parallel Kappa temperature (\( T_{\|,K} \)) can be calculated from \( w_\kappa \):

\[
 w_\kappa = \sqrt{\frac{2\kappa - 3}{\kappa k_B T_{\|,K}}}. \tag{12}
\]
In fact, the temperature obtained with the Kappa fit ($T_{\parallel,e}$) is much lower than the temperature obtained with a Maxwellian fit. The $T_{\parallel,e}$ for the $\kappa = 5$ case falls within the range of observations shown by Tao et al. (2016) and MacNeil et al. (2017).

A Maxwellian model was chosen because it most accurately represents new observations of the strahl provided by PSP. For the measured energy range, up to 800 eV, the strahl VDF cutting through the parallel direction shows no signs of high energy tails. This is not strictly true for the strahl measured by Helios, especially at larger distances, neither for the strahl observed at 1 au (Tao et al. 2016; MacNeil et al. 2017; Wilson et al. 2019b). The radial evolution of the strahl modeled by a Kappa function is presented by Štverák et al. (2009). They report the increase of $\kappa$ values at smaller distances from the Sun, reaching $\sim$14 at 0.3 au (64.5 $R_S$). For large $\kappa$ values, a Kappa distribution tends toward a Maxwellian; therefore, the PSP observations of a Maxwellian-like strahl VDF below 60 $R_S$ were not unexpected.

On the other hand, the increase of $\kappa$ for small distances (Štverák et al. 2009), and the measured Maxwellian-like strahls by the PSP, could be an instrumental artifact. Closer to the Sun, the total electron temperature is larger; therefore, the unaltered instrument energy span becomes relatively smaller than farther from the Sun. We are only able to measure a smaller portion of the strahl VDF, which could be missing the high energy tails—the most important part for distinction between a Kappa and a Maxwellian VDF.

The idea that the strahl electrons carry the information about the temperature of the electrons at the exobase is a part of exospheric solar wind models, as they initially do not take into account collisions or wave–particle interactions (Jockers 1970; Lemaire & Scherer 1971).

Two studies investigated the relation between the temperature of the supra-thermal electron population observed at 1 au, and the coronal temperature so far. Both of them make use of the oxygen charge-state ratio ($O^+ / O^+$) measurements as an estimate for the coronal electron temperature. In the study by Hefti et al. (1999), a clear correlation between the strahl parallel temperature and the oxygen charge ratio was observed, while MacNeil et al. (2017) present a data interval where the correlation is present and a data interval where it is not. Unfortunately, neither of the two spacecraft presented in this work provide us with a measurement of oxygen state ratios.

But this measurement will be provided by the Solar Orbiter, the new probe exploring the inner heliosphere launched on 2020 February 10 (Müller et al. 2013).

Another parameter strongly correlated with the temperature of the solar corona, which is often used as an indicator of the solar wind origin, is the solar wind velocity (Lopez & Freeman 1986). The solar wind originating from the center of the coronal holes, where the proton plasma temperature is higher than that of electrons, has a higher terminal velocity than the wind coming from the edges of the coronal holes. Figures 6 and 7 agree with this global picture as they display a clear anticorrelation between $T_{\parallel}$ and the solar wind proton velocity.

Using the sub-spacecraft points in combination with the synoptic map of the Sun allows us to follow the time evolution of the $T_{\parallel}$ and compare it with the current state of the solar corona (Figure 8). Through comparison with the PFSS modeling of the magnetic field line topology during the first orbit of PSP presented in the study by Badman et al. (2020), we crudely separated the strahl temperature data into three bins. The coldest $T_{\parallel}$ ($T_{\parallel} < 75$ eV) were observed at times when measured magnetic field lines appear to connect to a bigger equatorial coronal hole encountered just after the first PSP perihelion. During the first encounter, when a period of high-speed solar wind implies connectivity to the smaller coronal hole (Figure 8(b)), the strahl temperatures appear a bit higher temperature, $75 \text{ eV} < T_{\parallel} < 85 \text{ eV}$. These values are in agreement with the coronal electron temperatures obtained via the spectroscopy technique presented by David et al. (1998) and Crammer (2002). They report the coronal hole electron temperature just above the solar surface to be $0.79 \text{ MK} (=68 \text{ eV})$, reach its maximum temperature at 1.15 $R_S$, stay below 1 MK (=86 eV), and decrease after (Figure 2 in the referred article). For the quiet equatorial corona, the temperatures appear to be higher, starting at 1 MK and increasing until they reach 3.16 MK (=272 eV) at 1.3 $R_S$.

This evidence lead us to believe that $T_{\parallel}$ indeed retains the information about the temperature of electrons at their origin. However, to be convinced that $T_{\parallel}$ is not just correlated with but equals to the coronal electron temperature, further analysis is required. As mentioned above, the exobase is not a discrete point above the solar surface but a continuous region over which the collisions become less and less important. Another thing one needs to account for is the energy-dependent scattering of the strahl electrons. The strahl was, for most of the measurements, observed to be narrow but still broader than what is expected from the simple collisionless model. For example, scattering by Coulomb collisions at only lower energies would result in a higher $T_{\parallel}$. The study of the effect of continuous exobase and Coulomb collisions making use of kinetic simulations BiCop (Landi & Pantellini 2001, 2003) is a current work in progress.

6. Conclusions

The PAW data obtained during the first two orbits of PSP agrees well with the results obtained from the Helios data set presented by Berčič et al. (2019). We find the same PAW dependence on $\beta_{\parallel}$: in high-$\beta_{\parallel}$ solar wind, the strahl appears broader than in the low-$\beta_{\parallel}$ solar wind. For the measured energy range, the PAW was found to decrease with electron energy reaching down to $30^\circ$ for the lower two $\beta_{\parallel}$ bins, representing the majority of measurements.

We present, for the first time, observations of $T_{\parallel}$ from both the PSP and Helios missions. An anticorrelation was found
between $T_{\parallel}$ and the solar wind velocity ($v_p$), while $T_{\parallel}$ was observed to be constant over radial distance ($r$). These findings lead us to conclude that the strahl carries information about the coronal electron temperature at the point of its origin and can be used as a good proxy for connectivity studies involving remote sensing and in situ data. In fact, the origins of the solar wind measured by PSP anticipated from the strahl temperature measurements compare very well to the ones obtained using a PFSS model presented by Bale et al. (2019) and Badman et al. (2020). Even though the measured values of $T_{\parallel}$ agree very well with the coronal electron temperatures measured with the spectroscopes on board the SOHO spacecraft (David et al. 1998; Cranmer 2002), we believe further analysis is required to confirm that $T_{\parallel}$ is a direct measure of the electron temperature in the corona.

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### Appendix A

**PAW—FOV Effects**

The combined FOV of SPAN-E instruments is not uniform (Kasper et al. 2016; Whittlesey et al. 2020). Electrons are detected by two instruments, and the azimuth anodes of each of them have two possible angular widths: 6° and 24°. Part of the full solid angle is not sampled and is part blocked by the heat shield (see Figure 1). We investigated how much the nonuniform FOV affects our data analysis.

We identified two extreme configurations of the magnetic field vector in the FOV. The measurement is the most precise when the magnetic field vector lies within part of the FOV covered by the small azimuth anodes of SPAN-A. The most problematic measurement of the strahl electrons happens when the magnetic field is aligned with the radial direction, because in this case, the strahl electrons get blocked by the heat shield, which is during the encounter time directed directly toward the Sun.

The results are presented in Figure A1. PAWs measured at low electron energies are independent of the configuration of the magnetic field in the FOV. However, the strahl electrons with higher energies during the first encounter appear ∼10° broader when the magnetic field lies outside of the FOV covered by the small anodes of SPAN-A. The variation is less pronounced during the second encounter.

![Figure A1](image.png)

**Figure A1.** Strahl PAW with respect to electron energy, separated into three bins according to location of the magnetic field vector in the FOV of the instruments. Bin edges are noted in the legend followed by a number of instances belonging to each bin. (a) Encounter 1, (b) Encounter 2.
Appendix B

PAW—Standard Deviation B

Another test was conducted to determine how much the variation of the magnetic field during the integration time of SPAN-E instruments affects our strahl PAW measurements. We calculated the standard deviation of a 294 Hz magnetic field measurement during each SPAN-E scan lasting 27.96 s for the first encounter. For the second encounter, the magnetic field was sampled with a cadence of 147 Hz, and the duration of one scan was set to 13.98 s.

Figure B1 shows PAWs separated into two groups according to the standard deviation of the magnetic field during the SPAN-E measurement. Another test was conducted to determine how much the strahl PAW with respect to electron energy, separated into two bins according to the standard deviation of the magnetic field during each SPAN-E scan lasting 27.96 s for Encounter 1, (a) Encounter 1, (b) Encounter 2.

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