Measurement of moment coupling in fretting fatigue experiments

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Abstract
Moment coupling in fretting fatigue experiments refers to the generation of moments when a shear force is applied, caused by the difficulty in designing fretting fatigue experiments where the shear is reacted out on the same plane as the contact. Digital Image Correlation is used to measure the effect of moment coupling, and a model is created to calculate the effect of the applied moment at any point during a loading cycle on near-edge contact properties. The effects of the changing contact pressure on the slip zone sizes are considered. Finally, the model derived is used to find a load cycle including the effect of normal contact force that creates a truly constant near-edge contact pressure distribution at one edge of the flat and rounded pad. Although the calibrations found in this paper are valid only for the specific rig and specimen geometry used in this paper, the method could be readily applied to other experiments.

Keywords
Contact mechanics, fretting, fatigue, solid mechanics, experimental techniques

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Introduction
Fretting fatigue occurs in contact problems in the presence of partial slip, meaning that some region of the contact is permanently stuck and some region of the contact is undergoing cyclical reversing slip. The contacts conditions resulting from fretting fatigue processes result in a region where cracks can initiate, which can eventually result in component failure. Understanding the effect of fretting fatigue on component lifetime is therefore essential for assemblies in which crack propagation from contacts could result in dangerous failures of components, such as the contacts present at the root of fan blades in aero engines.1

Experimental investigations in fretting fatigue are primarily based on matching the contact stress fields in a real problem with those in a much simpler geometry which is easier to analyse, such as a dog bone specimen in contact with a pair of profiled pads.2 To match the stress field in the dog bone to that in the real geometry there are four loads that must be controlled; the differential bulk tension $\sigma$ and shear load $Q$ which affect the shear stress distribution along the contact interface, while the normal load $P$ and moment $M$ which affect the contact pressure distribution.3

When contact problems are analyzed in half plane theory it is assumed that $P$ and $Q$ are applied through a point located at the centre of the pad and on the plane of the contact, so that their effects are uncoupled. In test machines it is difficult to react out the shear in the plane of the contact, so instead it is often supported at a fixed distance from the contact plane. In addition there is always a finite projection of the pad which behaves like a short cantilever in the presence of a tip shear force. This results in ‘moment coupling’, where the application of a shear load results in the simultaneous application of a moment. This presents a particular problem when ‘flat and rounded’ or ‘square’ pad geometries are used, as the application of a moment can result in significant changes in the normal contact pressure adjacent to the edge of contact, or, in extreme cases, the lifting off of one edge of the punch.4

Experimental setup and measurements
Experiments were conducted using the rig, Figure 1, located in the Servo-Hydraulic Laboratory at the University of Oxford. This test apparatus was
originally designed to perform high temperature experiments to simulate the conditions present in gas turbine engines, which resulted in the support frame being extremely large to ensure there was sufficient thermal isolation between the specimen and the hydraulic components. This has resulted in significant problems with rigidity, and, in order to allow for the installation of a furnace, the shear force is reacted out through the plate springs (A) at a significant distance from the contact interface (B).

An overview of the rig showing the load paths present is given in Figure 2. The left and right actuators apply loads to each end of the dogbone specimen, while a third actuator at the bottom of the rig applies the pad normal load, \( P \). The shear load applied to each pad is therefore given by \( \frac{1}{2}(F_L - F_R) \). The shear force applied to each pad is supported through four plate springs attached to each pad holder, designed in such a way that they are compliant in the direction of the normal load. The significant distance between the plane of the contact between the pad and dogbone and the springs supporting the applied shear load results in the generation of a coupled moment, \( M \), at the contact interface.

In tests a pair of flat and rounded pads with 15 mm central flat and 1.5 mm corner radius were used. These were pressed into a steel dogbone 30 mm high with a thickness of 6 mm. The ends of the dogbone were serrated to provide a fatigue resistant connection to the actuators, and pin joints were subsequently fitted between the dogbone and the horizontal actuators to prevent twisting of the dogbone due to any slight misalignments (not present in Figure 1). This pad and dogbone geometry was used throughout all subsequent measurements.

It is not possible to measure the coupled moments or contact pressure directly, so instead the surface displacements of the pad and dogbone are measured, and the moment calculated from the resulting deflections. Digital image correlation (DIC) was used to measure these displacements; in this method a speckle pattern is applied to the surface of the components, a series of pictures of the component is taken during the load cycle and software is used to derive the motion and deflection of the components. Digital image correlation has previously been applied to fretting fatigue experiments, for the measurement of coefficient of friction, slip and strains, for example.

It was suspected that there would be a small amount of coupling between the application of the normal load and the moment, due to distortion of the frame. A series of digital image correlation measurements was therefore taken. The pads and dogbone were prepared with a speckle pattern using black and white matt spray paint. A Point Grey camera was used to capture greyscale images of the dogbone and pads at 2 frames per second at a resolution of 4240 × 2824 pixels. The digital image correlation software MatchID was used to check the quality of the speckle pattern and to process the collected images. The loads given in Table 1 were used, to cover fully those arising in typical fretting fatigue tests. To ensure that only partial slip was present a maximum shear force of 15% of the normal load was applied to each pad. The actuator at the left hand of the rig was set to maintain a fixed load of 15 kN, while the actuator at the right hand side of the rig was cycled to apply the shear load.

| Normal load (kN) | Shear load amplitude (kN) | Plane strain equivalent normal load (N/mm) | Plane strain equivalent shear load amplitude (N/mm) |
|------------------|--------------------------|-------------------------------------------|-----------------------------------------------|
| 5                | 1.5                      | 833                                       | 125                                           |
| 10               | 3                        | 1667                                      | 250                                           |
| 15               | 4.5                      | 2500                                      | 375                                           |
| 20               | 6                        | 3333                                      | 500                                           |
| 25               | 7.5                      | 4167                                      | 625                                           |
| 30               | 9                        | 5000                                      | 750                                           |
| 35               | 10.5                     | 5833                                      | 875                                           |
After the images were processed the DIC software was used to track the vertical displacements of two regions of points located adjacent to each edge of the pad. For each of these regions the vertical displacement of the edge of the pad was measured and the difference between the two measurements was used, in conjunction with the known width of the pad, to calculate the angle of pad tilt. By matching the image with the maximum amount of pad tilt to the peak of the load cycle it is possible to generate a plot of pad tilt vs applied shear load, an example of which is shown below in Figure 3, for the case of 20 kN applied normal load. It was found that for all 7 cases investigated the angle of pad tilt varied linearly with applied shear force.

In order to ascertain how the angle of pad tilt per unit shear varied with applied normal load a linear model was fitted to the measurements for several values of normal load, and the gradient of the line found, given in Table 2. It was revealed that there was no systematic variation in the amount of pad tilt per unit shear load with changing normal load, the value being fixed at a mean value of 0.0039 degrees/kN.

### Table 2. The measured coupling between pad tilt and shear load at each of the applied normal loads.

| Normal load (kN) | Pad tilt per kN shear (degrees/kN) |
|-----------------|-----------------------------------|
| 35              | 0.0037                            |
| 30              | 0.0040                            |
| 25              | 0.0039                            |
| 20              | 0.0040                            |
| 15              | 0.0040                            |
| 10              | 0.0041                            |
| 5               | 0.0035                            |
| Average         | 0.0039                            |

**Calculation of equivalent moment and creating a calibration**

In order to convert the measured angle of pad tilt into an equivalent applied moment a closed form solution for a tilted flat and round contact subject to normal load and moment is used, derived in Andresen et al. This was implemented in a MATLAB script, kindly provided by Dr H. Andresen. The magnitude of the moment developed will depend on the normal load and the angle of pad tilt, so for each value of the applied normal load the equivalent moment was calculated at steps of 0.001 degrees over the full range of pad tilt experienced at each value of normal load. It was found that, over the range considered, the magnitude of the moment varied linearly with pad tilt for all 7 loading cases considered. An example plot for the case of a normal load of 35 kN is shown in Figure 4.

The final thing considered is the effect of the normal load on the magnitude of the moment coupling. For each value of normal load the moment per degree of pad tilt was noted, and the results are shown in Table 3. Although there is some variation of the moment with applied normal load, with higher normal loads implying a greater degree of coupling, this effect was extremely small, with the difference between the 5 kN case and the 35 kN case less than
It was therefore decided to ignore this effect and assume that the relationship between moment and pad tilt was constant, with the value simply given by the mean of the calculated values.

It is now possible to create a calibration that allows us to express the magnitude of the coupled moment developed as a function of the applied shear load. Starting with the data in Table 2 we can express the relationship between the angle of pad tilt and the plane strain equivalent shear as

\[ h = 4.68 \times 10^{-5}S \]  

(1)

where \( h \) is the angle of pad tilt in degrees and \( S \) is the plane strain equivalent shear load, in \( \frac{N}{mm} \) (force per unit pad thickness). Note that in order to convert the actuator shear load to its per pad equivalent it must be divided by 2, as the actuator shear force is simultaneously applied to two pads. Likewise using the data in Table 3 it is possible to write the coupled moment as a function of the angle of pad tilt

\[ M = 88300 \]  

(2)

where again \( \theta \) is measured in degrees and \( M \), the moment per unit pad thickness is given in units of \( \frac{Nmm}{mm} \). Combining the two expressions we therefore arrive at equation (3), which characterizes the behaviour of the rig over the full range of loads used in conjunction with this pad and dogbone geometry.

\[ M = 4.13S \]  

(3)

In order to validate this expression the equivalent moment was calculated at the point of maximum shear force for each of the 7 load cases that were measured. This moment, in conjunction with the normal load are used as inputs to the tilted pad solution, and it was found that the implied angle of pad tilt was the same as the maximum angle of pad tilt measured with DIC.

**Effect of the coupled moment**

Having found an expression that allows us to calculate the magnitude of moment developed in a fretting fatigue experiment we now wish to consider briefly what effect it will have on the contact, first by finding its effect on the contact pressure distribution, and finally on the size of the slip zones. In the following calculations we will consider only the behaviour of

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**Table 3.** The effect of varying the normal load on the magnitude of the moment coupling.

| Normal load (kN) | Plane strain equivalent moment per degree pad tilt ((Nmm/mm)/degree) |
|------------------|---------------------------------------------------------------|
| 35               | 89100                                                        |
| 30               | 88900                                                        |
| 25               | 88600                                                        |
| 20               | 88400                                                        |
| 15               | 88100                                                        |
| 10               | 87800                                                        |
| 5                | 87400                                                        |
| Average          | 88300                                                        |

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**Figure 4.** A plot of the relationship between pad tilt and moment for an applied normal load of 35 kN.
the pad for the 35 kN normal load case as a representative example.

The load on the dogbone will vary between two points as the shear is cycled. At the first point the left actuator (when viewed from the front, as in Figure 1) will be applying 15 kN of tension while the right is applying 4.5 kN, resulting in an overall shear force of 10.5 kN acting to the left and a bulk tension of 25 MPa. At the second load point the left actuator will be applying 15 kN tension while the right actuator applies 25.5 kN, resulting in an overall shear force of 10.5 kN acting to the right and a bulk tension of 83.3 MPa.

**Effect on contact pressure**

Figure 5 shows a direct comparison between the contact pressure for the flat and rounded pad both including and excluding the effect of the moment, at the point in the load cycle where the right actuator is applying a tension of 4.5 kN. The plots here show only the outermost regions of the contact, $-0.95 \leq \frac{z}{w} \leq -1$ and $0.95 \leq \frac{z}{w} \leq 1$, where the width of the contact is $2w$. As expected it can clearly be seen that the application of the moment results in an increase in contact pressure at one edge of the contact, and a decrease at the other. The peak contact pressure is given in the first row of Table 4. The tilting of the punch will also affect its geometry, and in doing so will change the location of the maximum pressure. This is given in the second row of the table. Furthermore as the pad tilts the half-width of the contact will increase at the high pressure end and reduce at the low pressure end, these effects are shown in the third row of Table 4, with the contact extent being measured from the centre of the flat. It is worth nothing that the overall width of the contact remains essentially unchanged as the moment is applied.

**Effect on slip zone size**

We will now briefly discuss what effect the application of the moment has on the size of the slip zones at each end of the contact, again for the 35 kN normal load case. The steady state slip zone size for a contact subject to varying moment, normal load, shear load

![Figure 5. A comparison of the contact pressure, including and excluding the effect of the coupled moment at each edge of the fretting pad.](image)

| Contact property             | No moment | Left Edge | Percentage change | Right Edge | Percentage change |
|-----------------------------|-----------|-----------|-------------------|------------|-------------------|
| Peak contact pressure, MPa  | 2770      | 2460      | -11.2%            | 3060       | +10.5%            |
| Location of maximum pressure from centre, mm | 7.530 | 7.540 | +0.13% | 7.520 | -0.13% |
| Contact extent, mm          | 7.600     | 7.590     | -0.13%            | 7.610      | +0.13%            |
and bulk tension can be found analytically, as analyzed in Andresen et al.\textsuperscript{11} The slip zone sizes found in this way are shown in Table 5, given in microns, and assuming a coefficient of friction of 0.55. It can be seen that the change in slip zone size is rather significant in this setup, as the change in the half width of the contact is of the same order of magnitude of the slip zone size.
Removing the effect of the moment

Calculating a load cycle

We now wish to create a loading cycle such that the effect of the moment is cancelled out at one edge of the contact. In the previous section we saw that when the shear load was acting to the left the left hand edge of the pad lifted off, and the contact pressure reduced. To counteract this we could therefore simultaneously increase the pad normal load when we apply the shear, such that the local contact pressure remains constant. We can treat the case when a shear load is applied to the right in a similar manner. The left hand edge of the pad ‘digs in’, and the contact pressure increases; we must therefore reduce the pad load to maintain a constant contact pressure.

It should be noted that it is only possible to cancel the effect of the moment coupling at one edge of the contact, and varying the normal load in this manner will increase the pressure variation at the other edge of the contact. In the majority of fretting fatigue experiments this is unlikely to be important because we are concerned with matching the near edge contact pressure only in the neighbourhood of crack nucleation. Most specimens are loaded with a combination of shear and bulk tension, the effects of which are additive at one edge of the specimen and subtractive at the other. For most tests we know at which edge of the contact failure will occur before starting the experiment.

In the following example we will match the contact pressure at the left hand edge of the contact by adjusting the peak contact pressure to that found in the no moment case. A MATLAB script is used with an iterative solver to find the appropriate change in normal load. Using this solver we arrive at the load cycle given in Table 6.

Figure 6 shows a three way comparison between the contact pressure for the idealised case where no moment is present, the contact pressure including the effect of the unwanted moment, and the contact pressure from the load cycle with the normal load correction. The top plots are for the case where the shear force is acting to the left, the bottom plots are for the shear acting to the right. As predicted it can be seen that by varying the normal load

| Contact property                  | No moment | Shear to left | Percentage change | Shear to right | Percentage change |
|-----------------------------------|-----------|---------------|-------------------|---------------|-------------------|
| Peak pressure, MPa                | 2769      | 2769          | –                 | 2769          | –                 |
| Contact extent (from C/L), mm     | 7.596     | 7.596         | 0.00%             | 7.597         | +0.01%            |
| Slip zone size, μm                | 22.315    | 22.184        | –0.59%            | 22.423        | +0.48%            |

Figure 7. The vertical deflection of each end of the pad during two load cycles for the 20 kN nominal normal load case.
appropriately an extremely close match in the contact pressure at the left edge of the contact may be achieved, but at the expense of a larger deviation at the right hand edge.

Table 7 contains a variety of contact properties, calculated for both the idealised no moment case and the moment corrected load cycle. It can be seen that in comparison to Tables 4 and 5 that the error is much smaller, in all cases being less than 1%, indicating a good match between the theoretical constant load cycle and the moment corrected cycle.

Experimental validation using DIC

The same DIC setup that was used to measure the magnitude of the moment coupling was used to check that varying the normal load created a constant contact pressure at one edge of the contact. The Test rig was set up with the same specimen and pad combination as used in the measurements, and were loaded with the derived varying normal load cycle. The vertical displacement of each corner of the pad was recorded over 2 load cycles.

Figure 7 shows a plot of the vertical displacement of each end of the pad for the 20 kN nominal normal load cycle. It can be seen that the varying normal load cycle has successfully removed the effect of the moment coupling at one end of the pad, with the vertical deflection being reduced to approximately zero.

Conclusion

Moment coupling – the development of a rocking moment as a shear force on the contact is applied - is an unavoidable feature of fretting fatigue tests. It can be reduced by careful design but cannot be fully eliminated. When modelling the behaviour at the edge of contacts in fretting fatigue it is important that the action of moment coupling effects are accounted for. A method of measuring the magnitude of the moment coupling is derived through the use of DIC and a closed form solution for flat and rounded contacts, and a way of accounting for the coupled moment is found. The effect of the coupled moment is found to be non-trivial, particularly its effect on the predicted slip zone sizes. A load cycle with varying normal load is used to offset the effect of the moment, then DIC is used to validate that the resulting load cycle results in a truly constant normal pressure at one edge of the contact. Through this procedure it is therefore possible to match the behaviour of an experiment to an analytically derived load cycle in rigs with variable normal load actuation.

Declaration of Conflicting Interests

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References

1. Tang H, Cao D, Yao H, et al. Fretting fatigue failure of an aero engine turbine blade. Eng Fai Anal 2009; 16: 2004–2008.
2. Hills DA and Nowell D. Mechanics of fretting fatigue – Oxford’s contribution. Tribol Int 2014; 76: 1–5.
3. Andresen H and Hills DA. A review of partial slip solutions for contacts represented by half-planes including bulk tension and moments. Tribology International 2020; 143: 106050.
4. Sackfield A, Truman CE and Hills DA. The tilted punch under normal and shear load (with application to fretting tests). Int J Mech Sci 2001; 43: 1881–1892.
5. Blades LE, Hills DA, Wormsen A, et al. 2020. Fretting fatigue design of subsea connectors: matching results between pairs of tests. In: Proceedings of the International conference on offshore mechanics and arctic engineering – OMAE, Volume 2A-2020, Article number V02AT02A039, American Society of Mechanical Engineers, USA.
6. Nesládek M, Spaniel M, Jurenka J, et al. Fretting fatigue – experimental and numerical approaches. Int J Fatigue 2012; 44: 61–73.
7. De Pauw J, De Waele W, Hojjati-Talemi R, et al. On the use of digital image correlation for slip measurement during coupon scale fretting fatigue experiments. Int J Solids Struct 2014; 51: 3058–3066.
8. Texier D, Atmani F, Bocher P, et al. Fatigue performances of FSW and GMAW aluminum alloys welded joints: competition between microstructural and structural-contact-fretting crack initiation. Int J Fatigue 2018; 116: 220–233.
9. Andresen H, Hills DA and Vázquez J. Closed-form solutions for tilted three-part piecewise-quadratic half-plane contacts. Int J Mech Sci 2019; 150: 127–134.
10. Andresen H. Frictional Half plane contacts in partial slip in the steady state, DPhil Thesis, Oxford University, UK, 2020.
11. Andresen H, Hills DA, Barber JR, et al. Steady state cyclic behaviour of a half-plane contact in partial slip subject to varying normal load, moment, shear load, and moderate differential bulk tension. Int J Solids Struct 2020; 182–183: 156–161.