Crystalline and magnetic structure of Ba$_2$CuO$_{3+\delta}$ investigated by x-ray absorption spectroscopy and resonant inelastic x-ray scattering

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Motivated by the recent synthesis of Ba$_2$CuO$_{3+\delta}$ (BCO), a high temperature superconducting cuprate with putative d$_{3z^2- r^2}$ ground state symmetry, we investigated its electronic structure by means of Cu $L_3$ x-ray absorption (XAS) and resonant inelastic x-ray scattering (RIXS) at the Cu $L_3$ edge on a polycrystalline sample. We show that the XAS profile of BCO is characterised by two peaks associated to inequivalent Cu sites, and that its RIXS response features a single, sharp peak associated to crystal-field excitations. We argue that these observations are only partially compatible with the previously proposed crystal structure of BCO. Based on our spectroscopic results and on previously published powder diffraction measurements, we propose a crystalline structure characterized by two inequivalent Cu sites located at alternated planes along the c axis; nominally trivalent Cu(1) belonging to very short Cu-O chains, and divalent Cu(2) in the oxygen deficient CuO$_x$ planes. We also analyze the low-energy region of the RIXS spectra to estimate the magnitude of the magnetic interactions in BCO and find that in-plane nearest neighbor superexchange exceeds 120 meV, similarly to that of other layered cuprates. Although these results do not support the pure d$_{3z^2- r^2}$ ground state scenario, they hint at a significant departure from the common quasi-2D electronic structure of superconducting cuprates of pure d$_{3z^2- r^2}$ symmetry.

I. INTRODUCTION

Since the discovery of high temperature superconductivity in cuprates\cite{1}, many efforts have been spent to provide a conclusive and generally accepted explanation of this phenomenon. Unfortunately, results obtained so far are only partially satisfactory\cite{2}.

The discovery of novel families of unconventional superconductors is extremely important to help distinguishing indispensable and unnecessary, or even competing, ingredients for superconductivity. In this respect, the recent synthesis of Nd$_{0.8}$Sr$_{0.2}$NiO$_2$, an infinite-layer superconducting nickelate, is extremely welcome\cite{3} and, despite dissimilarities with superconducting cuprates, the paradigm that a 3$d^9$ ground state with d$_{x^2-y^2}$ orbital symmetry of the hole is key to achieve high temperature superconductivity is further strengthened\cite{4-7}. Li et al., however, challenged this belief by synthesising Ba$_2$CuO$_{3+\delta}$, a high temperature superconducting cuprate with putative d$_{3z^2- r^2}$ ground state symmetry\cite{8}.

Most cuprates are layered materials, with superconducting CuO$_2$ planes intercalated by blocking layers that act as charge reservoirs. In their antiferromagnetic, insulating parent compounds the ground state has predominant d$_{x^2-y^2}$ symmetry due to the sign of the tetragonal crystal field acting on the Cu$^{2+}$-derived electronic states. Moreover, it has recently been suggested that the larger the energy splitting between the d$_{x^2-y^2}$ and the d$_{3z^2- r^2}$ states, the higher the superconducting critical temperature\cite{9}. Ba$_2$CuO$_{3+\delta}$ (BCO) is supposedly isostructural to the prototypical (La$_{2-x}$Ba$_x$)CuO$_4$ high-temperature cuprate superconductors, which adopt a K$_2$NiF$_4$-type structure, where a sizeable elongation of the CuO$_6$ octahedra in the $c$ axis direction typically stabilizes a ground state with d$_{x^2-y^2}$ symmetry. In BCO, instead, it was suggested that Cu-O bonds might be shorter out of plane than in plane, leading to a ground state with predominantly d$_{3z^2- r^2}$ character. This scenario is intriguing, because it undermines the relevance of the d$_{3z^2- r^2}$ ground state for high temperature superconductivity and, therefore, motivates further investigations. At a theoretical level, a mechanism for the pairing that heavily relies on the significant weight of both d$_{x^2-y^2}$ and d$_{3z^2- r^2}$ orbitals at the Fermi energy has been recently proposed\cite{11}. Experimentally, instead, little has been done besides the initial work of Li et al.\cite{8}.

Here we probe BCO by means of x-ray absorption spectroscopy (XAS) and resonant inelastic x-ray scattering (RIXS) at the Cu $L_3$-edge to set constraints on its crystal, magnetic and electronic structure. Experimental limitations due to the use of a polycrystalline sample prevented us from exploiting all the possibilities offered by these techniques; in particular, we could not investigate the angular and polarization dependence of XAS and RIXS cross-sections and determine the symmetry of the ground and excited states in BCO, as done in the past for other cuprates\cite{12}. Nevertheless, we show that our results are only partially compatible with the crystal structure previously proposed for BCO and propose an alternative, consistent with our and previous measurements.
II. EXPERIMENTAL METHODS

Our powder sample of Ba$_2$CuO$_{3+\delta}$ ($\delta \approx 0.2$) is characterized by a superconducting critical temperature $T_c \approx 70$ K and was synthesised according to the procedure described in Ref. 8.

XAS and RIXS spectra were collected at the I21 beam line of the Diamond Light Source (Didcot, UK). XAS measurements were carried out in total fluorescence yield mode. RIXS spectra were measured with an overall energy resolution of approximately 55 meV. The x-ray beam spot size was approximately $3 \times 20 \mu$m$^2$. The polarization of the incident photons was vertical in the laboratory reference frame and perpendicular to the scattering plane. The scattering angle $2\theta$ was kept fixed at 154°.

The polycrystalline sample was compressed in a pellet, mounted on the sample holder and then sealed in a vacuum suitcase in the protected atmosphere of a glovebox. The vacuum suitcase was brought to the beam line and connected onto the sample load-lock. In order to expose a fresh sample surface, the pellet was cleaved at a vacuum pressure lower than $10^{-7}$ mbar. All measurements were carried out at a temperature of 20 K and a base vacuum pressure lower than $5 \times 10^{-10}$ mbar.

III. RESULTS

We report in Fig. 1(a) the x-ray absorption profile of BCO across the Cu $L_3$ absorption edge. It shows two distinct features (to be discussed in the following) at approximately 932.9 eV and 934.6 eV, respectively.

We collected RIXS spectra for incident photon energies in the energy window corresponding to the XAS spectrum and show the results in Fig. 1(b). The strong, narrow feature at constant zero energy loss is the elastic line, while higher energy loss features correspond to inelastic excitations which depend on the incident photon energy. The intense peak at approximately 1.5 eV energy loss is maximised in the vicinity of the first peak in the XAS spectrum ($\sim 932.9$ eV) and its position is rather constant as the incident photon energy is scanned. In agreement with a number of RIXS studies on cuprates 12,13, these features are assigned to crystal field (or $dd$) and charge-transfer excitations. A broader and weaker feature is observed at higher energy losses: it is strongest at incident photon energies corresponding to the second peak in the XAS spectrum and partially displays a fluorescence-like behaviour as seen, for example, in YBa$_2$Cu$_3$O$_{6.99}$ (see Supplemental Materials of Ref. 14).

A closer inspection of the RIXS data is provided in Fig. 2, which shows two vertical cuts of the RIXS map of Fig. 1(b). The overall shape of the spectra is markedly different: in particular, the RIXS spectrum taken at low incident photon energy (blue) shows a single, narrow peak at 1.6 eV energy loss, whereas the RIXS spectrum taken at high incident photon energy (red line) is characterized by two, broad features at approximately 2 and 4 eV. In addition, we highlight in the inset the presence of a feature at approximately 0.2 eV, which resonates at the lower energy peak in the XAS spectrum.

Before moving to the discussion of the experimental results, we note that the polycrystalline BCO sample was found to be rather inhomogeneous as observed with both XAS and RIXS. The black dashed lines in Figs. 1(a) and 2 correspond to XAS and RIXS spectra, respectively, taken on a different area of the sample. The inhomogeneity is demonstrated in the maps of Fig. 3: in panel (a) we show the spatial dependence of the relative intensity change of the two XAS peaks through the ratio

$$R = \frac{I(932.7 \text{ eV}) - I(934.6 \text{ eV})}{I(932.7 \text{ eV}) + I(934.6 \text{ eV})},$$

where $I(X)$ is the XAS intensity at energy $X$; in panel (b) we show the spatial dependence of the full width at half maximum of crystal-field excitations in the RIXS spectra. The two maps show a clear correlation, and the first peak in the XAS is larger in the part of the sample where the crystal field transition in RIXS is sharper. The length scale of the spatial variations amounts to a few tens of microns. We are aware of the fact that these samples are particularly sensitive to air exposure: different grains might have been chemically stabilized differently, leading to spatial variations of doping and composition.
Figure 2. RIXS spectra of polycrystalline BCO measured at incident photon energies of 932.7 (solid blue, dashed black) and 934.6 eV (solid red line), corresponding to the vertical lines in Fig. 1, respectively. The dashed black curve is the RIXS spectrum acquired on the region of the sample corresponding to the dashed black XAS profile of Fig. 1(a). The inset shows a close-up view of the low energy loss window.

In agreement with literature\(^8\), we here focus our attention on the region of the sample where the second XAS peak is weaker. Moreover we use the RIXS spectra excited at the first XAS peak, thus selecting mostly Cu\(^{2+}\) sites in the “good” phase.

Figure 3. Spatial dependence of (a) the ratio between the two peaks in the XAS spectrum of Fig. 1(a) and (b) the width of the 1.6 eV excitation in the RIXS spectrum of Fig. 2.

Figure 4. RIXS spectra of powder BCO (as in Fig. 2, blue), compared to single-crystalline LSCO\(^{16}\) (red) and CCO (yellow line) reference systems, normalized to the spectral weight of the dd excitations.

IV. DISCUSSION

We start the discussion by commenting on the Cu L\(_3\) edge XAS spectrum of BCO: irrespective of its detailed interpretation, the presence of two distinct features suggests the presence of two, non-equivalent Cu sites in the system. As established in the literature on cuprates, the first and second XAS peak in Fig. 1(a) can be associated to nominal Cu\(^{2+}\) and Cu\(^{3+}\) species, respectively\(^{14,15}\). However, in the structure previously proposed for BCO all the Cu sites are considered to be equivalent, as summarized in Fig. 6(a) and Tab. I. The double XAS peak, in that scenario, would be possible only in the (unlikely) case of a strong charge discommensuration. Here we have explored other scenarios consistent both with the powder diffraction patterns shown in Ref. 8 and with the present XAS (and RIXS) data that suggest the existence of two inequivalent Cu sites, in analogy to YBCO. To keep the analogy with YBCO we label Cu(1) and Cu(2) the Cu\(^{3+}\) and Cu\(^{2+}\) site respectively. Based on the maps of Fig. 1 and the spectra of Fig. 2 we will concentrate on RIXS spectra excited at 932.7 eV, which correspond to selecting Cu(2) sites only.

In Fig. 4, we compare the crystal field excitations in superconducting BCO and two prototypical cuprate systems, i.e., the single-layer superconductor La\(_{2−x}\)Sr\(_x\)CuO\(_4\) (LSCO, \(x = 0.15\))\(^{16}\) and the infinite-layer insulator CaCuO\(_2\) (CCO).

Crystal field (or dd) excitations arise from the redistribution of electrons within the atomic 3d shell through the RIXS process. For a Cu\(^{2+}\) ion, a single particle approach is justified and dd excitations simply correspond to transitions between crystal field split states\(^{12,13}\). The symmetry and energy of 3d states is thus determined by the geometrical arrangement of the nearest neighbour oxygen ions around the central Cu\(^{2+}\) ion, whereas the Cu-O bond distances set the magnitude of the splitting. The scattering geometry and polarization dependence of the RIXS cross-sections for dd excitations have been successfully used to determine the symmetry of the ground and excited states of several cuprates\(^{12,17,18}\). In particular, the assignment of dd excitations in CCO is as follows: the peaks at approximately 1.7, 2.0 and 2.7 eV correspond to transitions from the \(d_{x^2−y^2}\) ground state to the
$d_{xy}$, $d_{yz/zx}$ and $d_{3z^2-r^2}$ excited states, respectively; in the case of LSCO, doping causes an overall broadening of the spectrum, but one can still appreciate that the energies of the $d_{xy}$ and $d_{yz/zx}$ transitions are similar to those in CCO, whereas the $d_{3z^2-r^2}$ excited state is found around 1.4 eV, in analogy to the single-layer insulating parent compound La$_2$CuO$_4$. We note that the energy of the $d_{xy}$ excited state is mainly dictated by the in-plane Cu-O bond distance, which is similar for LSCO (1.91 Å) and CCO (1.93 Å). Instead, the energy of the $d_{3z^2-r^2}$ excited state is mostly determined by the out-of-plane coordination of Cu$^{2+}$: in LSCO, the out-of-plane Cu-O bond distance is 2.46 Å, while the infinite-layer structure of CCO features CuO$_4$ plaquettes with no apical oxygens (also shown in Fig. 4), which pushes the $d_{3z^2-r^2}$ excited state to higher energies.

Figure 5 shows the energy of the Cu 3$d$ states as a function of the out-of-plane/in-plane Cu-ligand distance. In the inset we show the 10$Dq$ energy as a function of the in plane Cu(2)-O bonds.

The RIXS spectrum of BCO is remarkably different from those of CCO and LSCO, and of all the layered cuprates studied so far. In particular, Fig. 4 suggests three main observations: $dd$ excitations in BCO are i) lower in energy than any other cuprate system; ii) sharper and iii) more symmetric than in LSCO.

Figure 5 shows the energy of the Cu 3$d$ states as a function of the ratio between the out-of-plane and in-plane Cu(2)-O distance obtained from simple crystal field considerations reported in Ref. 22: we consider an hydrogen-like model for Cu$^{2+}$ surrounded by six $-2e$ point charges at the corners of an octahedron and an effective nuclear charge $Z_{eff} = 6.7$ such that $10Dq = 1.8$ eV for Cu(2)-O$_{in-plane}$ = 1.91 Å (as in La$_2$CuO$_4$ (LCO)) and provides a qualitative picture of the energy level splitting. In the case of an octahedron compressed along the $z$ axis, the ground state has the $d_{3z^2-r^2}$ symmetry of the only 3$d$ hole of Cu$^{2+}$, whereas for an elongated octahedron the ground state is characterized by a $d_{x^2-y^2}$ symmetry. In both cases, the energy of the other 3$d$ states is strongly affected by the effective Cu(2)-O$_{out-of-plane}$/Cu(2)-O$_{in-plane}$ ratio. The crystal field model suggests that the energy of the $d_{3z^2-r^2}$ and the two-fold degenerate $d_{yz/zx}$ states is mostly influenced by the Cu(2)-O$_{out-of-plane}$ distance, while 10Dq, i.e. the energy difference between the $d_{x^2-y^2}$ and $d_{xy}$ orbitals, is mostly dictated by the Cu(2)-O$_{in-plane}$ distance, as reported in the inset of Figure 5. The in-plane Cu(2)-O bond distance is considerably larger in BCO (2.00 Å) than in LSCO and CCO, thus explaining the overall lower energy of $dd$ excitations in BCO than in the other cuprates. Indeed, the decrease of 10$Dq$ with the Cu(2)-O$_{in-plane}$ distance of Figure 5 can be fit to a power decay with exponent -4.5; one can then rescale 10$Dq$ of LCO with the lattice parameter of BCO and obtain a value $\sim 1.8 \text{eV} \times (2.00 \text{Å}/1.91 \text{Å})^{-4.5} \approx 1.5$ eV, in agreement with our observations.

Beyond the information on the average crystal field energy and Cu-O distances, RIXS spectra can be used to learn more about the crystalline structure of BCO. For the sake of simplicity in the discussion, we consider a nominal $\delta = 0.25$, corresponding to the formula with integer stoichiometric coefficients Ba$_8$Cu$_4$O$_{13}$. In this case, the in-plane oxygens should have a fractional occupancy of $\frac{13}{16}$, i.e., the Cu ions are coordinated to 4.5 oxygens, on average, instead of 6 as in LCO. Supposing a random

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Table I. Principal parameters for the crystal structure of BCO ($\delta = 0.25$) for the crystal structure reported in Ref. 24 and shown in Fig. 6(a).

| label | symbol | mult. | Wyckoff |
|-------|--------|-------|---------|
| Ba(1) | Ba     | 4     | e       |
| Cu(1) | Cu     | 2     | a       |
| O(1)  | O      | 4     | e       |
| O(2)  | O      | 4     | c       |

Space group : I4/mmm (# 139)
$a = b = 4.003 \text{Å}, c = 12.942 \text{Å}$

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Figure 6. Crystal structure of BCO as reported in Ref. 8 (a) and as proposed in this work (b). Green, blue and (partially filled) red balls represent Ba, Cu and (partially occupied) O sites.
distribution of oxygen vacancies and ignoring, for a moment, the distinction between Cu(1) and Cu(2) sites, one would expect a variety of coordinations for Cu ions, with 3, 4, 5 and 6 oxygen ligands, and a consequential distribution of dd excitation energies. Indeed, it has been shown that disorder leads to broadening of the dd excitation multiplet in RIXS. Therefore, the observation ii) of a very narrow crystal field excitation feature in the RIXS spectrum of BCO does not seem to be consistent with a highly disordered system. Moreover, the average coordination of Cu imposes that a large number of CuO4 plaquettes should form in BCO, therefore contributing to the RIXS spectrum with an excitation at high energy losses (≥ 2.5 eV), similarly to the d_{3z^2-r^2} transition in CCO. The observation iii) of a very symmetric line shape excludes the presence of such a high energy peak, therefore suggesting that most of the Cu ions have a coordination number larger than 4, at least for the disordered sites Cu(2) probed by RIXS.

Recently, Liu et al. confirmed that oxygen vacancies prefer to reside in the planar rather than the apical sites and suggested alternative, more stable crystals structures; in particular, they considered a 2×2×1 supercell and calculated the energies associated to 26 possible crystal structures with various arrangements of 6 oxygen vacancies (corresponding to the δ = 0.25 phase we are considering here). They found that the most favourable structures contain 6 and 4 oxygens within layers at fractional coordinates z = 0 and z = 0.5, respectively. Indeed, those structures imply three inequivalent Cu sites: one 6-fold coordinated at z = 0, and two 4-fold coordinated at z = 0 and z = 0.5. To comply with our experimental evidence of 2 and not 3 Cu sites, we propose a modified structure, shown in Fig. 6(b), that still respects the property of having 6 oxygens at z = 0 and 4 at z = 0.5 as in Ref. 25. Moreover, it features only two inequivalent Cu sites, Cu(2)2+ and Cu(1)3+, within the z = 0 and z = 0.5 layers, respectively. And the Cu2+ ions, contributing to the RIXS spectra of Fig. 4, are 5-fold coordinated in pyramids, while Cu3+ ions, silent for RIXS at 932.7 eV incident photon energy, are 4-fold coordinated in plaquettes. It is important to note that, in our model, the plaquettes in the z = 0.5 layer do not form long chains but are equally and randomly distributed between the ac and the bc planes to respect the tetragonal symmetry of the structure. This condition is also needed in consideration of the XAS spectral shape. In fact, when the Cu-O-Cu bond angle is 180°, like in chains of corner-shared CuO4 plaquettes, the inter-plaquette electron hopping is maximized and non-local processes are able to screen the core hole in Cu3+ L3 XAS and the corresponding peak in the XAS spectrum becomes very broad and barely visible. Instead, when the Cu-O-Cu bond angle is close to 90° the inter-plaquette hybridisation is strongly suppressed and non-local ligand electrons cannot take part in the core-hole screening, which results in a sharp and well defined Cu3+ peak. The XAS of BCO showing two well defined peaks clearly agrees with the latter scenario and indicates that the plaquettes must be disordered, though all oriented perpendicular to the ab plane. Tables II reports additional information on the crystal structure of BCO that we are proposing here.

| label | symbol | mult. | Wyckoff | x  | y  | z  | occupancy |
|-------|--------|-------|---------|----|----|----|-----------|
| Ba(1) | Ba     | 8     | n       | 0.250 | 0.000 | 0.144 | 1.000 |
| Ba(2) | Ba     | 8     | o       | 0.000 | 0.750 | 0.357 | 1.000 |
| Cu(1) | Cu     | 4     | j       | 0.250 | 0.000 | 0.500 | 1.000 |
| Cu(2) | Cu     | 4     | g       | 0.000 | 0.750 | 0.000 | 1.000 |
| O(1)  | O      | 2     | a       | 0.000 | 0.000 | 0.000 | 1.000 |
| O(2)  | O      | 4     | e       | 0.250 | 0.250 | 0.000 | 1.000 |
| O(3)  | O      | 8     | o       | 0.000 | 0.750 | 0.144 | 1.000 |
| O(4)  | O      | 8     | n       | 0.250 | 0.000 | 0.357 | 1.000 |
| O(5)  | O      | 2     | d       | 0.000 | 0.000 | 0.500 | 0.500 |
| O(6)  | O      | 2     | c       | 0.000 | 0.500 | 0.500 | 0.500 |

Table II. Principal parameters for the crystal structure of BCO (δ = 0.25) as proposed in this work and shown in Fig. 6(b).

Figure 7. Simulated pXRD patterns for the crystal structures reported in Fig. 6(a) and (b).

The crystal structure originally proposed for BCO was obtained by fitting its experimental powder x-ray diffraction (pXRD) pattern. The corresponding simulated pXRD pattern is reported in Fig. 9 as a solid blue line, which we use as a reference for comparison with the simulated pXRD pattern of the crystal structure we propose in this work: it turns out that the pXRD patterns of the crystal structures reported in 6(a) and (b) largely overlap and are indistinguishable at a first sight. When the intensities are plotted on a logarithmic scale (inset), little discrepancies that become apparent are below the detectability limit of the pXRD experiment (red line), estimated from the (in)visible peaks in the experimental data. Therefore, we believe that the structure we propose here is as compatible as the one proposed originally with the currently available experimental pXRD pattern.
Having established that the crystal structure of Fig. 6(b) is compatible with previous pXRD measurements, we now discuss implications on the electronic properties of BCO. We expect that the superconductivity takes place in the $z = 0$ layer, while the $z = 0.5$ layer plays the role of charge reservoir, in analogy to YBCO. Therefore, we would like to discuss in more detail the ground state symmetry of the Cu(2) ions. As shown in the inset of Fig. 6(b) the Cu$^{2+}$ ions are coordinated in pyramids, having their base in the $ac$ plane. In a regular pyramid coordination the degeneracy of the Cu 3$d$ orbitals is lifted in similar way as for an elongated octahedron. However, the fact that the pyramid apex is lying in the $z = 0$ plane implies that, to a first approximation, the hole is in the $d_{x^2-y^2}$ orbital. The $d_{x^2-y^2}$ orbital with only two lobes in the $ab$ plane while the two other lobes sticking out along the $c$ axis, is different from the $d_{x^2-y^2}$ orbital with all four lobes lying in the $ab$ plane, usually found in other cuprate superconductors. This should affect the strength of the magnetic couplings, which could be different along the $a$ and $b$ directions. It has to be noted, however, that the compressive distortion along the $c$ axis (with the Cu-O distances being equal along $a$ and $b$ but shorter along $c$) causes a further reduction of the point group symmetry of the Cu(2) ions from $D_{4h}$ to $D_{2h}$, with two consequences: the degeneracy of all 3$d$ states is removed, including that of the $d_{xy}$ and $d_{yz}$ orbitals, and the $d_{x^2-y^2}$ orbital is mixed up with the $d_{3y^2-r^2}$ orbital, adding some in-plane character to the hole wave function. With this in mind, we calculated the RIXS cross-sections\textsuperscript{12} for a generic $\cos \alpha \left| d_{x^2-y^2} \right> + \sin \alpha \left| d_{3y^2-r^2} \right>$ ground state and fit the experimental RIXS spectra to the corresponding four excited states in order to extract the mixing parameter $\alpha$ and the crystal field splittings. Unfortunately, the problem is ill-defined because the $dd$ peak is very narrow and symmetric, and the decomposition is not unique. Therefore, at this stage, we can only state that the ground state has a mixed character of $d_{x^2-y^2}$ and $d_{3y^2-r^2}$ orbitals but we cannot determine the degree of admixture, for which the use of a single crystalline sample would be necessary. When single crystals of BCO will be available both XAS and RIXS will provide much more insightful information on the crystalline and electronic structure thanks to the polarization dependence of cross sections.

Finally, we discuss the low-energy excitations in BCO. The RIXS spectrum of Fig. 8 is simultaneously fit to three symmetrical, energy resolution-limited curves (grey lines) and one asymmetrical curve (dashed red line); in agreement with existing literature on cuprates\textsuperscript{28,29}, the peaks at 60 and 110 meV are tentatively assigned to phonons and the peak at 180 meV to magnetic excitations (paramagnons)\textsuperscript{30,31}. Based on this interpretation, we will try in the following to give an estimate of the magnetic interactions in BCO.

The proposed $ab$-plane crystal structure of BCO is shown in the inset of Fig. 9(b), where Cu-O-Cu superexchange paths exist between nearest-neighbour Cu$^{2+}$ ions along three bonds only, and might be different along the $a$ and $b$ directions. The fourth magnetic bond is broken by the systematic absence of oxygen ions, thus preventing the system from forming the square magnetic lattice common to all layered cuprates. Magnetic excitations are in general highly dispersive, i.e., their energy depends on the magnitude and orientation of the transferred momentum, so precautions should be taken before drawing conclusions on magnetic interactions because, for a powder sample, the RIXS signal is averaged over the fraction of reciprocal space accessible by the available momentum transfer. Assuming isotropic (Heisenberg) antiferromagnetic couplings $J_a$ and $J_b \leq J_a$ between nearest-neighbour spins 1/2 along the $a$ and $b$ directions, respectively, we calculated the structure factor of magnetic excitations using linear spin wave theory, as implemented in SpinW\textsuperscript{32}. The results are reported in Fig. 9 for $J_b = J_a = J$: the momentum transfer dependence of the magnetic structure factor for a powder sample is shown in panel (a) to be bounded at $1.5J$, as one should expect from simple considerations; a cut at 0.91 Å\textsuperscript{-1} momentum transfer, corresponding to performing RIXS at $2\theta = 154^\circ$ scattering angle, as in our experiment, is reported in panel (b) and mostly consists of a single peak at an energy of 1.5$J$. When, by supposing an in-plane anisotropy of the superexchange interaction due to the lower density of oxygen ions along $b$, the magnetic coupling along the $b$ direction is progressively decreased with respect to $J_a$, the upper boundary of the powder-averaged magnetic structure factor decreases to approximately $J_a$. The comparison with our RIXS data for BCO, then, suggests a superexchange coupling constant $120 \leq J_a \leq 180$ meV, in line with the magnitude of the antiferromagnetic superexchange interaction in most
cuprates. We note that the BCO structure proposed here is very similar to that chosen by Wang et al. to study the magnetic and electronic structure and superconductivity of this material with the $t-J$ model in the co-called brick-wall lattice of CuO$_{1.5}$ planes.

Figure 9. (a) Simulated momentum dependence of the magnetic structure factor and (b) its cut at 0.91 Å$^{-1}$, corresponding to scattering angles of $\theta = 154^\circ$ for powder BCO. The considered nearest-neighbours superexchange interactions can be seen from the $ab$-plane crystal structure of BCO, also shown.

V. CONCLUSIONS

In our work, we probe the electronic structure of BCO by combining XAS and RIXS techniques. We argue that our measurements are only partially consistent with the crystal structure previously proposed for BCO and propose an alternative structure that is compatible with both previous pXRD measurements and recent theoretical calculations. The proposed structure features two inequivalent Cu sites and naturally justifies the double peak structure in the XAS profile. Moreover, the systematic vacancies of oxygens in the $z = 0$ layer explains the absence of a high-energy crystal field excitation in the RIXS spectra, and leads to an estimated nearest neighbor superexchange intergrals in BCO in line with most common cuprates, i.e., of the order of 150 meV. Interestingly the in plane antiferromagnetic square lattice is expected to characterize the superconducting planes of BCO as in the other cuprate superconductors, despite the loss of local $C_4$ symmetry in the magnetic interaction in BCO.

From the structure here proposed, we predict that superconductivity occurs in the $z = 0$ layer and the ground state is an admixture of $d_{x^2-y^2}$ and $d_{3x^2-r^2}$ orbitals. Unfortunately, our present experimental data on powder BCO are insufficient to determine the degree of this mixture, but will possibly serve as a basis for future investigations on single crystal BCO samples. More in general, and beside the specific case of BCO, we demonstrate that XAS and RIXS can be usefully employed to set constraints on the plausible crystal structure of a newly synthesised oxide.

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