Neutral hydrogen (H I) gas content of galaxies at $z \approx 0.32$

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ABSTRACT

We use observations made with the Giant Metrewave Radio Telescope (GMRT) to probe the neutral hydrogen (H I) gas content of field galaxies in the VIMOS VLT Deep Survey (VVDS) 14h field at $z \approx 0.32$. Because the H I emission from individual galaxies is too faint to detect at this redshift, we use an H I spectral stacking technique using the known optical positions and redshifts of the 165 galaxies in our sample to co-add their H I spectra and thus obtain the average H I mass of the galaxies. Stacked H I measurements of 165 galaxies show that $\gtrsim 95$ per cent of the neutral gas is found in blue, star-forming galaxies. Among these galaxies, those having lower stellar mass are more gas rich than more massive ones. We apply a volume correction to our H I measurement to evaluate the H I gas density at $z \approx 0.32$ as $\Omega_{\text{HI}} = (0.50 \pm 0.18) \times 10^{-3}$ in units of the cosmic critical density. This value is in good agreement with previous results at $z < 0.4$, suggesting no evolution in the neutral hydrogen gas density over the last $\sim 4$ Gyr. However the $z \approx 0.32$ gas density is lower than that at $z \approx 5$ by at least a factor of two.

Key words: galaxies: evolution – galaxies: ISM – radio lines: galaxies.

1 INTRODUCTION

A long-standing challenge in galaxy formation and evolution is to address the relationship between stars, gas and metals in galaxies. In particular, the mechanisms that supply the fuel for star formation in galaxies are unclear. Neutral atomic hydrogen (H I) gas, a primary ingredient for star formation, is a key input to understand how various processes govern galaxy formation and evolution. Cold gas like the neutral atomic hydrogen gas has been only poorly inventoried, whereas in contrast astronomers have measured the properties of the stellar components of galaxies such as star formation rate density (SFRD) and stellar density over cosmic time (e.g. Hopkins 2004; Hopkins & Beacom 2006; Marchesini et al. 2009; Madau & Dickinson 2014) much better.

Two observational approaches have proven to be effective in measuring the abundance of neutral hydrogen in the Universe. In the high-redshift Universe ($z > 2$), saturated Lyman $\alpha$ absorption arising from intervening systems seen against bright background sources, viz. the so-called damped Lyman $\alpha$ absorption systems (DLAs), measures the abundance of H I gas. Recently, large DLA surveys have been used to make high precision measurements of cosmic H I gas density ($\Omega_{\text{HI}}$) (e.g. Prochaska, Herbert-Fort & Wolfe 2005; Noterdaeme et al. 2009, 2012; Zafar et al. 2013; Crighton et al. 2015; Neeleman et al. 2016; Sánchez-Ramírez et al. 2016; Bird, Garnett & Ho 2017). These studies show that there exists at least two times more hydrogen gas in the high redshift Universe than in the local Universe. However, this technique is not practical in the low-redshift Universe because the ultraviolet (UV) transition lines of the Lyman series are not observable at $z \lesssim 1.5$ with ground-based telescopes and because of the very low incidence rate of DLAs in the local Universe. This leads to large uncertainties in the low-redshift H I abundance measurements derived from DLAs (e.g. Rao, Turnshek & Nestor 2006; Meiring et al. 2011).

In the local Universe, the amount of H I gas has been quantified exclusively by H I 21-cm emission. In particular, blind H I surveys such as H I Parkes All Sky Survey (HIPASS, Meyer et al. 2004) and Arecibo Fast Legacy ALFA (ALFALFA, Giovanelli et al. 2005) have covered a large volume of sky. These surveys allow accurate measurements of the local H I mass function and H I mass density of galaxies, which are in good agreement (Zwaan et al. 2003, 2005; Martin et al. 2010; Haynes et al. 2011). However, this approach has been limited to $z \lesssim 0.2$ because the current generation of radio telescopes is too insensitive to detect the feeble H I emission from distant populations of galaxies (Hoppmann et al. 2015).

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2 OPTICAL DATA

2.1 Target field selection

We selected one of three independent fields in the VIMOS VLT Deep Survey (VVDS)-Wide (Le Fèvre et al. 2005; Garilli et al. 2008; Le Fèvre et al. 2013), VVDS 14h, as the target field for H I 21-cm observations with the GMRT. The VVDS-Wide was designed to measure redshifts of galaxies with a limiting magnitude of $I_{AB} = 22.5$ out to $z \sim 1$ using the VIsible Multi-Object Spectrograph (VIMOS) on the European Southern Observatory (ESO) Very Large Telescope (VLT).

For our observations, the GMRT frequencies restricted the redshift range to $0.30 < z < 0.34$. In this limited redshift interval and field of view, there were only 41 reliable redshifts in the VVDS-Wide catalogue available for the radio data analysis. This is an insufficient number of redshifts to obtain a strong H I 21-cm signal using the stacking technique. Moreover, the VVDS has a low spectral resolution of $R = 230$ with a dispersion $7 \text{ Å pixel}^{-1}$, resulting in a large redshift uncertainty of $\sim 300 \text{ km s}^{-1}$ (Le Fèvre et al. 2005). This increases the uncertainty in the stacked H I signal and the subsequent measurements. To obtain more redshifts with higher precision, we used two optical telescopes with multi-object optical spectrographs: Hectospec (Fabricant et al. 1998, 2005) on the 6.5-m MMT and AAOmega (Saunders et al. 2004b; Smith et al. 2004; Sharp et al. 2006) on the 3.9-m Anglo–Australian Telescope (AAT).

2.2 Sample selection

The effective field of view for our optical spectroscopic observations corresponds to a circular field of one degree diameter, smaller than the total area of 2.2 deg$^2$ surveyed for the VVDS 14h field in the original VVDS-Wide. This field has good optical imaging coverage in both $R$ and $I$ bands along with Sloan Digital Sky Survey (SDSS) imaging, and the SDSS archive contains 16 881 possible spectroscopic targets. This number is too large to reasonably observe with Hectospec and AAOmega, and many of the targets are too faint to obtain redshifts with these instruments. However, using the existing photometry, one can apply the SDSS star–galaxy criteria and a series of colour cuts to select objects likely to be galaxies in our desired redshift range.

Comparing SDSS magnitudes and redshifts obtained from the VVDS project, we investigated various colour distributions of galaxies in the VVDS 14h field. Fig. 1 (left) shows the colour–colour locus of objects in the redshift range covered by the GMRT observations. The $g - r$ vs $r - i$ colour cuts indicated in the figure were used to make target lists of $r < 21$ galaxies for the MMT and AAT spectroscopic observations. For galaxies with $r > 21$, an additional requirement of $g - r \leq 1.25$ was imposed because spectroscopy of such faint galaxies is unlikely to yield redshifts unless the galaxy has emission lines, and blue galaxies are more likely to have emission lines.

The bright galaxies were assigned the highest priority for observing because they were more likely to yield redshifts. Applying the selection criteria, 2240 target galaxies were selected for Hectospec observations and a target list of 2161 galaxies was made for AAOmega observations. Included in the lists were 41 galaxies that already had VVDS redshifts, but had large uncertainties. Seven of these are red and faint and would not otherwise have been included in the sample. (See right-hand panel of Fig. 1.)

2.3 Observations and data reduction

Hectospec and AAOmega are ideal spectrographs for efficiently obtaining a large number of galaxy redshifts because they have large fields of view and many fibres to simultaneously obtain spectra. The Hectospec instrument has 300 fibres and a field of view one degree in diameter. Wavelength coverage is 3700–9200 Å at 1.2 Å pixel$^{-1}$ and $R \sim 1000–2000$ (Fabricant et al. 1998, 2005). MMT observations of six fibre configurations were carried out in queue observing mode over five nights between 2011 February and April with a 1.5 hr exposure time (divided into three 0.5 hr exposures for cosmic ray removal) for each fibre configuration. 1526 of 2240 target galaxies, corresponding to $\sim 68$ per cent of our sample, were successfully observed.

The Hectospec spectra were processed through a semi-automatic pipeline developed specifically for Hectospec and based on IRAF scripts (Mink et al. 2007). It includes standard calibration with bias, dark and flat-fielding followed by wavelength calibration with comparison lamp exposures, then followed by subtracting night-sky emission lines. After sky lines were removed, each spectrum was cross-correlated against a set of templates of various galaxy spectra using RVSAO (Kurtz et al. 1992; Kurtz & Mink 1998), an IRAF add-on package developed at the Smithsonian Astrophysical Observatory (SAO)$^5$. This procedure yielded redshifts with quality 3 or better.
Figure 1. Left: colour–colour diagram for the VVDS 14h field. Yellow stars show objects in the VVDS catalogue having 0.30 < z < 0.34, and grey points show catalogue objects outside this redshift range. Dashed lines show the colour selection criteria adopted to select targets for the MMT and AAT observations. Right: colour–magnitude diagram for galaxies selected for spectroscopy. The bright sample is shown by red closed circles and the faint blue sample by blue open circles. The gap in the bright sample at g − r ≈ 1.25 reflects galaxy colours, not sample selection. Faint, red objects (black triangles) had pre-existing VVDS spectra.

for 1296 galaxies. The quality flags are defined by visual inspection as numbers from 5 to 0:

flag 5: 100 per cent convincing redshift with high SNR multiple emission or absorption lines.
flag 4: Reliable redshift with a mixture of strong and weak spectral lines.
flag 3: Probable redshift showing a couple of spectral lines with low SNR.
flag 2–0: Rejected.

The spectra of target galaxies unobserved by the MMT were taken using the AAOmega, a dual-beam and multifibre spectrograph mounted on the 3.9-m AAT at Siding Spring Observatory (SSO). AAOmega allows for the simultaneous observation of 392 targets including science objects, sky positions and guide stars over a two-degree field using 2dF fibre positioner (Lewis et al. 2002). AAOmega provides R = 1300 with a dispersion of 1 Å pixel\(^{-1}\) (Saunders et al. 2004b; Smith et al. 2004; Sharp et al. 2006) using the 5700 Å dichroic.

The AAT observations were done on 2011 June 1–4 in the wavelength range 3700 Å to 9000 Å with an exposure time of 2.5 hr for each of the four fibre configurations. The data were reduced using dedicated software developed at the Australian Astronomical Observatory (AAO)\(^6\) called 2dfdr (Croom, Saunders & Heald 2004; Sharp & Birchall 2010). 2dfdr applies a standard sequence of data reduction to extract a one-dimensional spectrum of each object from two-dimensional images taken from AAOmega: bias subtraction, flat-fielding, fibre trace fitting and wavelength calibration. Then the redshifts were derived with the interactive cross-correlation software package RUNZ (Saunders, Cannon & Sutherland 2004a), assigning the same redshift quality flags as used for Hectospec redshifts. The spectra yielded 344 reliable redshifts out of 1398 galaxies targeted. The success rate was lower than that of the MMT/Hectospec because bright targets had already been observed by Hectospec, and the AAOmega targets were therefore fainter, and the weather at the telescope was poor.

2.4 Redshift measurements

Redshift measurements for both instruments are based on cross-correlation methodology (Tonry & Davis 1979). The calculated redshift uncertainties include statistical and systematic effects: noise, calibration errors and template mismatching. Tonry & Davis (1979) and Kurtz & Mink (1998) give more detail. As seen in Fig. 2, redshift measurements from both observatories have mean uncertainty

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\(^6\) http://www.aao.gov.au/2df/aaomega/aaomega_2dfdr.html
of $\sim 30$ km s$^{-1}$. This is important for H I stacking because it narrows the velocity window needed for co-adding the H I spectra.

The combined observations give a total of 1640 galaxy redshifts (see Table 1), of which 184 or 11 per cent are within the GMRT wavelength range corresponding to $0.30 < z < 0.34$. Fig. 3 shows the appearance of these galaxies.

Subsequent to our observations, the VVDS project released the final catalogues of its surveys (Le Fèvre et al. 2013). The VVDS 14h field is included in the VVDS-Wide survey and the catalogue has 60 objects within the GMRT beam and frequency coverage. Of these, 15 galaxies have reliable (based on its own quality flag, $zflag \geq 3$) redshifts not already known from our observations. The addition of redshifts from the final VVDS catalogue increased the total number of galaxies available to be co-added to 199.

### 2.5 Galaxy classification

Galaxies with optical redshifts in the GMRT range were classified into two subsamples—early type and late type—based on the dominance of absorption or emission lines. Initial classification was based on the templates used during the cross-correlation procedure for deriving redshifts, and all classifications were verified by visual inspection of the spectra. Galaxies with emission lines such as [O ii] and H$\alpha$, i.e. typical emission lines seen in spectra of star-forming galaxies, were classified as late-type. Those with strong absorption lines, e.g. Ca H and K, without emission lines were classified as early-type. Of the 184 galaxies observed by the AAT and the MMT, 34 were classified as early-type and 150 galaxies were classified as late-type. Visual inspection of the additional spectra from the

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7 Nine galaxies were observed at both telescopes and their redshifts agree.

8 An additional 11 galaxies have VVDS redshifts with low quality and are not included.

9 The maximum correction was 0.17 magnitude.

10 Mean corrections in individual bands were 0.35–0.77 magnitudes.
Table 1. Redshift catalogue of the VVDS 14h field taken from the AAT and MMT observations. The full table in machine-readable form is available online.

| SDSS object ID | R.A. (J2000) | Dec. (J2000) | Redshift ($z$) | Quality flag | Instrument |
|----------------|--------------|--------------|----------------|--------------|------------|
| 588010880382534322 | 13:57:36.12 | 5:31:47.7 | 0.320 044 ± 0.000 065 | 4 | Hectospec |
| 587729159509639373 | 13:57:05.62 | 4:49:05.6 | 0.320 850 ± 0.000 095 | 4 | Hectospec |
| 588010880382534003 | 13:57:29.44 | 5:29:08.1 | 0.321 540 ± 0.000 080 | 4 | AAOmega |
| 587729160046707183 | 13:59:05.01 | 5:14:19.2 | 0.322 960 ± 0.000 090 | 4 | AAOmega |
| 588010879845793833 | 13:58:46.00 | 5:06:15.9 | 0.322 980 ± 0.000 080 | 4 | AAOmega |
| 588010879308792391 | 13:57:41.24 | 4:41:23.2 | 0.323 292 ± 0.000 139 | 4 | Hectospec |
| 588010879308792194 | 13:57:33.63 | 4:43:08.7 | 0.323 530 ± 0.000 080 | 4 | AAOmega |
| 588010879308792394 | 13:57:41.28 | 4:41:21.2 | 0.323 720 ± 0.000 184 | 3 | Hectospec |
| 587729159509639598 | 13:57:04.37 | 4:52:56.9 | 0.324 770 ± 0.000 080 | 4 | AAOmega |
| 588010879308923480 | 13:59:05.97 | 4:44:26.6 | 0.325 410 ± 0.000 112 | 4 | Hectospec |
| 587729159509901597 | 13:59:15.32 | 4:45:24.9 | 0.325 543 ± 0.000 081 | 4 | Hectospec |
| 587729159509901676 | 13:59:15.91 | 4:45:58.9 | 0.325 547 ± 0.000 068 | 5 | Hectospec |

Figure 3. SDSS r-band thumbnail images of 184 sample galaxies in the VVDS 14h field that have $0.30 < z < 0.34$ from Hectospec and AAOmega spectroscopic observations and lie within the GMRT beam coverage. The size of each thumbnail image is 10 arcsec by 10 arcsec. They are ordered by increasing the $r$ magnitude.
beam coverage of the VVDS 14h field along with the positions of the catalogued galaxies with redshifts in the GMRT frequency band. Galaxies within the 10 per cent beam level were used for the subsequent HI spectral stacking analysis. The redshift distribution of the stackable galaxies within the GMRT frequency range is shown in Fig. 6. 46 per cent of the total sample is included in the lower sideband, while the rest lies in the upper sideband of the old correlator.

3.2 Data reduction

3.2.1 Calibration

Data reduction was conducted primarily with the Common Astronomy Software Applications (CASA, McMullin et al. 2007)1 following standard procedures: flagging; calibration; self-calibration; and imaging. Before implementing CASA for calibration and subsequent processes, we ran an automated flagging and calibration software developed for the GMRT data, the so-called FLAGCAL, to automatically search and discard corrupted data caused by malfunctioning antennas and radio frequency interference (RFI; Prasad & Chengalur 2012; Chengalur 2013). Assuming that true visibilities vary smoothly with time and frequency, the corrupted data due to RFI and instrumental errors can be identified by their deviant behaviours from the expected smoothness. To apply this approach, the data should be corrected for different antenna gains. FLAGCAL carries out calibration and flagging in an iterative way: calibration parameters were derived and applied to the raw data and then the data were inspected to find and remove corrupted data, followed by iterations of this procedure of calibrating and flagging with increasingly stringent criteria.

After editing away bad data via FLAGCAL, the visibilities were imported into CASA for the main data reduction procedures. Owing to the different frequency configurations, the pre-2011 and 2011 data sets were processed separately although the same data reduction procedure was used. Each of the 21 d was individually calibrated, keeping separate the two sidebands in the 2008 and 2009 data. Then all data sets were concatenated for computation of the final continuum images and data cubes. The data were inspected again using CASA visualisation tools, and additional flagging was performed as required. For calibration, bandpass calibration was first determined with flux and phase calibrators, and then calibration for flux and phase with 3C 147, 3C 286 and PKS 1345+12 was done with the central 80 channels of a total 128 channels in each sideband, avoiding channels severely affected by RFI. Science data to which all calibration solutions had been applied were split and inspected again followed by continuum imaging to check whether there remained bad data that could cause artefacts in the continuum image. After additional bad data found from this inspection were flagged, each data set was self-calibrated with six bright radio continuum sources in the VVDS 14h field to diminish residual amplitude and phase errors.

To make continuum Images of each sideband for self-calibration, we used 100 out of 128 channels in each sideband. These were averaged in groups of 10 adjacent channels to form 10 sub-bands of 1.25 MHz each to be used in gridding in the $uv$ plane in preparation for imaging. These bands are sufficiently narrow to avoid bandwidth smearing across our field of view. For self-calibration, a total of four loops were repeated in each sideband: two phase self-calibration loops and two amplitude & phase self-calibration loops. All self-calibrated 2008–2009 data were concatenated based on sideband, and self-calibration was carried out again with the entire combined data to ensure consistency over all the data observed on different days. For 2011 data, the data reduction sequence was the same as the 2008–2009 data: initial editing with FLAGCAL; calibration; self-calibration; concatenation; and self-calibration.

The data used in the final reduction were inspected to check how much data have been flagged due to RFI. Fig. 7 shows the frequency range observed by the GMRT is severely affected by RFI and instrumental failure. While more than 50 per cent of the data taken in 2008 and 2009 were flagged, the 2011 data were somewhat less contaminated by RFI, losing ~42 per cent to flagging. The upgrade of the GMRT backend systems to the software correlator likely contributes to this improvement in RFI mitigation. Having 50 per cent of the data remaining after all flagging is equivalent to having 21 of the 30 GMRT antennas working perfectly for the whole observation.

3.2.2 Continuum map

The final continuum map has a ~1 deg field of view (FoV) extending out to the 10 per cent beam level of the GMRT primary beam. To make the map we concatenated all data including the 2011 observations. In order to avoid bandwidth smearing, double sideband data used 100 channels with averaging every 10 channels and the single band data were also averaged with every 10 of 190 channels. The pixel size for imaging was 0′′85, and the ‘‘robust’’ weighting parameter (Briggs 1995) was set to zero, corresponding to a compromise between natural and uniform weighting.

When making continuum images as well as spectral data cubes at arcsec resolution, the one degree FoV of the VVDS 14h field is large enough to require a wide-field imaging algorithm. Unlike one-dimensional interferometer arrays such as the WSRT, the GMRT is two-dimensional and has non-coplanar baselines. The effect of the non-coplanar line-of-sight components (w-term) of the interferometer baselines has been one of the factors limiting wide-field imaging quality, though it can be ignored for small-field

\[ \text{http://casa.nrao.edu} \]
Figure 5. SDSS r-band negative image of the VVDS 14h field. Red circles mark galaxies with $0.30 < z < 0.34$ measured from our observations. Blue squares mark galaxies within the same redshift range measured by the VVDS-Wide survey. The central solid circle corresponds to the primary beam diameter (HPBW) of 31.2 arcmin at 1076 MHz. The outer dashed circle, 57 arcmin in diameter, represents the 10 per cent level of the GMRT beam.

imaging. However, the effect is no longer negligible as the imaging size required by current and future radio telescopes increases. To deal with the effect of the $w$-term on wide-field imaging, there are currently two commonly used algorithms: faceting (Cornwell & Perley 1992) and $w$-projection (Cornwell, Golap & Bhatnagar 2008).

The CASA imager is capable of implementing both algorithms.

For continuum imaging and creating the spectral data cube of the VVDS 14h field, the $w$-projection algorithm was applied in CASA because this has superior performance in speed and dynamic range to the faceting algorithm (Cornwell et al. 2008). Fig. 8 shows continuum images of bright sources $\gtrsim 13$ arcmin away from the phase centre. As seen in the top panel, the $w$-term effect results in errors around bright sources in the continuum image. Applying the $w$-projection algorithm, these disappear as seen in the bottom panel, and the peak signal-to-noise ratio (SNR) of the brightest source in the image increases by 4.7 times. The weaker, distorted sources to the lower right in the images are recovered cleanly in the bottom panel by applying $w$-projection.

Using bright sources with high SNR in the continuum maps, the astrometric accuracy of the GMRT data was checked by matching them against their positions in the VLA FIRST survey catalogue (Becker, White & Helfand 1995). The offset between the two coordinates is $\sim 0.48$ arcsec on average which is less than the image pixel size of 0.85 arcsec. The maximum measured offset for a single object was 1 arcsec, which is smaller than the GMRT synthesised beam size of 3.4 arcsec $\times$ 2.3 arcsec. The root-mean-square (rms) noise level of the continuum map is 15.07 $\mu$Jy beam$^{-1}$.

3.2.3 Spectral data cube

To obtain the final spectral data cubes, the radio continuum has to be subtracted from the spectral $uv$ data. Two methods were used sequentially to achieve this end. Firstly, clean component models of continuum sources were directly Fourier-transformed and then subtracted from the $uv$ domain using the CASA task ‘uvsub’. After creation of the spectral image cube by transforming the visibilities for each channel to its image plane, the small residual continuum flux that remained after the clean components subtraction was removed by subtracting a linear fit to the spectrum for each spatial pixel of the cube using the CASA task ‘imcontsub’. That is, a spectral data cube was made from the continuum-subtracted $uv$ data, and then the linear fit was applied to the data cube to measure and subtract the residual continuum flux. Three final data cubes were made: two-sideband (LSB and USB) data cubes each with 128 channels...
from 2008–2009 data and one data cube with 256 channels from the 2011 single-band (GSB) data. Each data cube has position axes spanning \( \sim 1.0 \times 1.0 \), and the frequency axis in the double-sideband data cubes has 128 channels corresponding to 4400 km s\(^{-1}\) in velocity space. The single-band data cube obtained from the new correlator has the same configuration except for having 256 frequency channels spanning 9100 km s\(^{-1}\). These data cubes were made with \( w \)-projection applied. The Briggs robustness parameter was set to zero, and a pixel size of 0.85 arcsec pixel\(^{-1}\) was used. The synthesized beam size of the final data cubes is \( \sim 3.5 \text{ arcsec} \times 2.4 \text{ arcsec} \), corresponding to \( \sim 16 \times 11 \text{ kpc}^2 \) at \( z \sim 0.32 \). This high spatial resolution helps to reduce the risk of confusion from companion galaxies, which complicates low-resolution H\(\text{I}\) stacking experiments using a single dish (e.g. Delhaize et al. 2013). The \( \text{rms} \) noise per channel in the double-sideband data cubes is \( \sim 153 \mu\text{Jy beam}^{-1} \), while the \( \text{rms} \) noise level of the single-continuous-band data cube is 190 \( \mu\text{Jy beam}^{-1} \).

4 STACKING H\(\text{I}\) 21-CM EMISSION

To make a direct detection of H\(\text{I}\) emission from an individual galaxy at 5\(\sigma\) significance in this GMRT observation, the galaxy would...
have to have an $\text{H}_\text{i}$ mass greater than $\sim 5.7 \times 10^{10} \, M_\odot$ within a 400 km s$^{-1}$ velocity profile and be smaller than the 3.5 arcsec synthesised beam. Such galaxies are rare in the local $\text{H}_\text{i}$ mass function (e.g. Zwaan et al. 2005; Martin et al. 2010), and it is unlikely that one would fall in the volume surveyed by the GMRT. Visual inspection of the data cubes yielded no obvious detection of any $\text{H}_\text{i}$ emitters. A search using DUCHAMP (Whiting 2012), an automated source-finding routine, was carried out through the entire spectral data cubes. No direct detection was found in this automated blind search, consistent with the visual inspection.

To reach an $\text{H}_\text{i}$ emission signal level with increased SNR, spectra from multiple galaxies were co-added, a process called ‘$\text{H}_\text{i}$ spectral stacking’ (Chengalur, Braun & Wieringa 2001; Zwaan, van Dokkum & Verheijen 2001). Redshifts obtained from the MMT/AAT optical spectroscopic observations were converted to the corresponding $\text{H}_\text{i}$ frequencies in the data cubes. As illustrated in Fig. 7, some channels of data cubes were severely contaminated by RFI, and it was necessary to exclude objects located in these bad channels. After removing these galaxies from the original sample of 199, 165 galaxies covering the range $0.3047 \leq z \leq 0.3370$ remained available for $\text{H}_\text{i}$ stacking. They are broken into subsamples of 32 early-type and 133 late-type galaxies, respectively.

The $\text{H}_\text{i}$ spectral stacking followed the methodology described by Rhee et al. (2013, 2016). In brief, individual spectra of sample galaxies were extracted and corrected for the primary beam attenuation based on the empirically measured GMRT primary beam pattern. Then each spectrum was shifted to the galaxy’s rest-frame velocity before co-adding all the spectra. The stacked spectrum was computed from a weighted average using the $\text{rms}$ noise of each gain-corrected spectrum to form a weight. A stacked spectrum was computed separately for the early-and late-type subsamples as well as a grand total spectrum for the full sample of 165 galaxies as plotted in Fig. 9.

The co-added spectra for each galaxy type can be converted to $\text{H}_\text{i}$ mass using the following equation (Wieringa, de Bruyn & Katgert 1992):

$$
\frac{M_{\text{H}_\text{i}}}{M_\odot} = \frac{236}{(1+z)^2} \left( \frac{D_L}{\text{Mpc}} \right)^2 \left( \int S_V \, \text{d}V \right) \text{mJy km s}^{-1},
$$

where $z$ is redshift, $D_L$ is the luminosity distance in units of Mpc and $\int S_V \, \text{d}V$ is the integrated $\text{H}_\text{i}$ emission flux in units of mJy km s$^{-1}$. To calculate the integrated $\text{H}_\text{i}$ flux in equation (1), we assumed the velocity window width of 400 km s$^{-1}$ within which all $\text{H}_\text{i}$ emission flux was integrated. This velocity window was estimated from the Tully–Fisher relation (Tully & Fisher 1977) using $B$ magnitudes converted from the SDSS magnitudes of our sample, giving mean $w_{20} = 275.5 \, \text{km s}^{-1}$ and maximum 492.1 km s$^{-1}$, where $w_{20}$ is the $\text{H}_\text{i}$ linewidth at 20 per cent of the peak flux. Allowing for redshift uncertainty of the sample galaxies, $2\sigma \sim 60 \, \text{km s}^{-1}$ along with the velocity profile widths ($w_{20}$) derived from the Tully–Fisher relation, the velocity width of 400 km s$^{-1}$ was used to calculate $\text{H}_\text{i}$ mass from the stacked $\text{H}_\text{i}$ spectra. Using different velocity widths from 350 km s$^{-1}$ to 500 km s$^{-1}$ makes no systematic difference in the average $\text{H}_\text{i}$ mass. The mean redshift 0.323 of stacked galaxies was used for this calculation and also for the luminosity distance in equation (1). To estimate the uncertainties of the stacked $\text{H}_\text{i}$ spectra, jackknife resampling (Efron 1982) was adopted.

The average $\text{H}_\text{i}$ mass was calculated separately for early-type and late-type galaxies (see Table 2). The early-type sample is unlikely to have a significant amount of $\text{H}_\text{i}$ gas, although the small number of galaxies stacked gives rise to a large statistical uncertainty. Most $\text{H}_\text{i}$ gas in this sample seems to reside in the late-type galaxies. This $\text{H}_\text{i}$ distribution can also been seen when comparing

\begin{figure}
\centering
\includegraphics[width=\textwidth]{co-added_hi_spectra.png}
\caption{Co-added $\text{H}_\text{i}$ spectra of galaxies in the VVDS 14h field. The left-hand panels show stacked $\text{H}_\text{i}$ spectra for different galaxy types as classified in Section 2.5. The blue horizontal dashed lines show 1$\sigma$ uncertainties of the stacked spectra. The right-hand panels show the co-added spectra rebinned to 400 km s$^{-1}$. The vertical dotted lines in all panels indicate the velocity window in which $\text{H}_\text{i}$ flux was measured and converted to $\text{H}_\text{i}$ mass.}
\end{figure}
the $\text{H} \text{I}$ gas richness of both populations using the ratio of $M_{\text{HI}}/L_B$. To do this, the $B$-band magnitude was transformed from the SDSS photometry, in particular $g - r$ colour and $g$-band magnitude according to the conversion relation provided on the SDSS website, and then converted to the $B$-band luminosity after Galactic dust extinction correction and $k$-correction. The $M_{\text{HI}}/L_B$ values are given in Table 2. The $M_{\text{HI}}/L_B$ ratio shows that the early-type subsample consists of gas-poor galaxies ($M_{\text{HI}}/L_B \lesssim 0.1$) as expected for an early-type population (Roberts & Haynes 1994). In contrast, the late-type subsample shows the typical $\text{H} \text{I}$ richness ($M_{\text{HI}}/L_B \approx 0.48$) of late-type galaxies.

In comparison samples at $z \sim 0.1$ and 0.2, Rhee et al. (2013) found $(M_{\text{HI}}/L_B) = 0.08 \pm 0.06$ for early-type galaxies and $(M_{\text{HI}}/L_B) = 0.31 \pm 0.06$ for late-type galaxies. The early-type galaxies at $z \sim 0.32$ likewise have $\text{H} \text{I}$ mass-to-light ratios consistent with zero although all the measurements have large uncertainties. Late-type galaxies appear to be more gas-rich at $z \sim 0.32$ than at $z \sim 0.1–0.2$ although the measurements overlap within the 1$\sigma$ error bars. While one may expect an evolutionary trend towards large gas mass-to-light ratios with increasing redshift, the error bars in our measurement are too large to make a definitive claim. Further, in comparison to the results from previous large blind HI surveys and an HI stacking analysis with large samples, the $M_{\text{HI}}/L_B$ ratio of our late-type sample does not appear significantly larger. Using the HIPASS catalogue with its optical counterparts identified from the 6dF Galaxy survey (6dFGS, Jones et al. 2004, 2009), Doyle et al. (2005) investigated the $M_{\text{HI}}/L_B$ ratios of a large number of galaxies in the local universe, showing the mass-to-light ratio for most of them is $1–2 M_\odot/L_\odot$. This is larger than for our late-type galaxies. Delhaize et al. (2013) also tested the $M_{\text{HI}}/L_B$ ratio of $\approx 18,000$ sources using an HI stacking technique. Their results have $M_{\text{HI}}/L_B$ ratios, which are in good agreement with Doyle et al. (2005) and decrease with redshifts out to $z \sim 0.1$. However, their $M_{\text{HI}}/L_B$ at their highest redshift ($z \sim 0.1$) is very similar to the $M_{\text{HI}}/L_B$ ratio that we measure for late types. The $M_{\text{HI}}/L_B$ measurement of their HIPASS data in an optical luminosity range similar to our mean luminosity is consistent with our $M_{\text{HI}}/L_B$ ratio.

Therefore the difference of $M_{\text{HI}}/L_B$ between the large surveys and our experiment seems attributable to sample size and selection effects.

To check whether the VVDS 14h galaxies are resolved by the GMRT synthesised beam, HI sizes of the sample galaxies were estimated using the relation between optical and HI sizes found by Broeils & Rhee (1997). They used optical $B$-band photometry

| Sample | $N_{\text{sample}}$ | $(M_{\text{HI}})\times 10^9 M_\odot$ | $(M_{\text{HI}}/L_B)$ |
|--------|---------------------|-----------------|-----------------|
| Early  | 32                  | $1.56 \pm 3.65 (0.4\sigma)$ | 0.06 $\pm 0.14$ |
| Late   | 133                 | $6.49 \pm 1.61 (4.0\sigma)$ | 0.48 $\pm 0.12$ |

Table 2. $\text{H} \text{I}$ mass measurements and $M_{\text{HI}}/L_B$ ratios of the VVDS 14h field galaxies for subsamples.
our spectroscopic redshifts. Galaxies with the largest stellar masses are mostly early-types. This is as expected and also shows that the spectroscopic classification is consistent with the stellar masses and colours derived from the photometry.

To explore the H\textsc{i} contributions from galaxies with different stellar masses, the late-type sample was divided into two subsamples based on the derived stellar mass: $M_\ast \leq 10^{9.5} \, M_\odot$ and $M_\ast > 10^{9.5} \, M_\odot$. The average H\textsc{i} mass of each subsample was measured by the same H\textsc{i} spectral stacking (see Fig. 13). Table 3 shows that the populations have similar H\textsc{i} gas amounts, but the low-mass sample is dominated by the gaseous component (H\textsc{i}), while stellar mass is dominant in the high-mass sample. A recent galaxy evolution model (Lagos et al. 2014) predicted this relation between stellar and gaseous mass because the galaxy population with $M_\ast \leq 10^{9.5} \, M_\odot$ has its gas mostly in the form of atomic hydrogen (H\textsc{i}) whereas the $M_\ast > 10^{9.5} \, M_\odot$ population has gas mostly in molecular form (H\textsc{ii}). The implication of this relation between stellar and H\textsc{i} mass is that the faintness of low-stellar-mass galaxies will bias optically selected H\textsc{i} surveys of neutral gas abundance.

6 GLOBAL H\textsc{i} GAS DENSITY EVOLUTION

6.1 H\textsc{i} Mass Density ($\rho_{\text{HI}}$)

The H\textsc{i} gas density ($\rho_{\text{HI}}$) in the VVDS 14h field can in principle be calculated from the total H\textsc{i} mass found by the GMRT divided by the comoving volume surveyed. However, calculating the effective volume considering survey incompleteness (and to a lesser extent excluded areas near bright foreground objects) is not trivial. The maximum volume available is bounded by the GMRT 10 per cent beam diameter ($\sim$0.95 deg) and the GMRT frequency range. After accounting for RFI and decreased effective bandpass (Fig. 7), this volume (calculated as prescribed by Hogg 1999) is $\sim$41 000 comoving Mpc$^3$. The detected H\textsc{i} density in this volume is $(2.31 \pm 0.60) \times 10^2 \, M_\odot \, \text{Mpc}^{-3}$ with the 133 late-type galaxies giving nearly all of it, $(2.11 \pm 0.53) \times 10^2 \, M_\odot \, \text{Mpc}^{-3}$. The H\textsc{i} contribution of the 32 early-type galaxies is $(0.12 \pm 0.31) \times 10^2 \, M_\odot \, \text{Mpc}^{-3}$, $<5$ per cent of the total H\textsc{i} density. While these values are strict lower limits on the H\textsc{i} density in the VVDS 14h field, they are not strict lower limits on the cosmic H\textsc{i} density because of cosmic variance. The original VVDS survey has cosmic variance $<5$ per cent for $z < 0.5$ (Driver & Robotham 2010). However, the narrow velocity range of our survey reduces the volume and increases the cosmic variance to $\sim$54 per cent.

Measuring the actual completeness of our spectroscopic survey is difficult, especially given the finding that low-mass systems appear to be very hydrogen rich as found in Section 5. Our selection criteria were deliberately biased to bright and late-type galaxies in order to obtain as many redshifts as possible. In order to account for both incompleteness and cosmic variance, we have normalized the observed H\textsc{i} density to the blue luminosity density ($L_\text{B}$) density. In effect, we use our measurements of $L(H\text{i})/L_\text{B}$ for the sample galaxies together with the known cosmic luminosity density in blue light. The method, described by Rhee et al. (2013, 2016), relies upon good measurements of the VVDS 14h field in the SDSS ugriz bands. While good ugriz photometric measurements are available for the entire galaxy sample, the luminosity function and density of the VVDS 14h field have not been computed and made available in the ugriz bands. Instead, we used a study by Ilbert et al. (2005), who

14 http://www.cfht.hawaii.edu/arnouts/lephare.html

15 http://cosmocalc.icrar.org/
Figure 13. Co-added HI spectra of two subsamples of late-type galaxies defined by stellar masses. The low-mass sample has stellar mass of $M_\star \leq 10^{9.5} M_\odot$, while the high mass sample contains $M_\star > 10^{9.5} M_\odot$.

Table 3. Average HI mass measurements for different stellar mass bins and the fraction of HI and stellar masses.

| Sample          | N$_{\text{sample}}$ | $\langle M_{\text{stellar}} \rangle$ | $\langle M_{\text{HI}} \rangle$ | $\langle M_{\text{HI}} \rangle / \langle M_{\text{stellar}} \rangle$ |
|-----------------|----------------------|---------------------------------------|---------------------------------|---------------------------------------------------------------|
| Late $M_\star \leq 10^{9.5} M_\odot$ | 72                   | $1.24 \pm 0.75$                       | $7.00 \pm 2.18$                 | $5.65 \pm 3.84$                                              |
| Late $M_\star > 10^{9.5} M_\odot$   | 61                   | $13.33 \pm 15.59$                     | $5.99 \pm 2.45$                 | $0.45 \pm 0.56$                                              |

Table 4. HI mass density and cosmic HI density. $N_{\text{sample}}$ is the number of galaxies that are co-added, $\langle M_{\text{HI}} \rangle$ is the average HI mass (in units of $10^9 M_\odot$), $\langle L_B \rangle$ is the mean $B$-band luminosity in units of $10^9 L_\odot$, $\rho_{L_B}$ is the luminosity density in units of $10^8 L_\odot Mpc^{-3}$, $\rho_{\text{HI}}$ is the HI density multiplied by the correction factor in units of $10^7 M_\odot Mpc^{-3}$ and $\Omega_{\text{HI}}$ is the cosmic HI density.

| $N_{\text{sample}}$ | $\langle M_{\text{HI}} \rangle$ | $\langle L_B \rangle$ | $\rho_{L_B}$ | $\rho_{\text{HI}}$ | $\Omega_{\text{HI}}$ |
|---------------------|---------------------------------|-----------------------|--------------|-------------------|-------------------|
|                     | $(10^9 M_\odot)$               | $(10^9 L_\odot)$      | $(10^8 L_\odot Mpc^{-3})$ | $(10^7 M_\odot Mpc^{-3})$ | $(10^{-3})$ |
| 165                 | $5.73 \pm 1.47$                | $16.20 \pm 0.11$      | $1.92 \pm 0.49$         | $6.79 \pm 2.48$         | $0.50 \pm 0.18$ |

computed the evolution of the galaxy luminosity function using the VVDS data in the $UBVRI$ bands. Ilbert et al. (2005) drew on data sets from two fields in the VVDS catalogue, though our VVDS 14h field was not included. We used the Ilbert et al. (2005) luminosity function and density around $z \approx 0.32$, assuming that variation of the luminosity function and density among the VVDS fields is insignificant at the redshift of interest (Garilli et al. 2008). $B$ magnitudes were obtained from the SDSS photometry as described in Section 4 and converted to $B$-band luminosities ($L_B$) after applying the Galactic dust extinction correction and $k$-correction. We then calculated $\rho_{L_B}$ for the entire sample applying the volume normalisation as following equation (5) of Rhee et al. (2016). All the values pertaining to this volume normalisation are listed in Table 4. The effect of the volume correction is to double the HI density. An additional correction to $\rho_{\text{HI}}$ is needed to account for galaxies too faint to have been included in our spectroscopic survey. The correction factor $f$ was estimated following the recipe of Rhee et al. (2013), which gives $f = 1.41$. The final $\rho_{\text{HI}} = (6.79 \pm 2.48) \times 10^7 M_\odot Mpc^{-3}$, almost triple the value computed by the simple volume division (see Table 4).

The above method of evaluating $\rho_{\text{HI}}$, intrinsically assumes that there is no strong variation of relative gas richness (i.e. $M_{\text{HI}}/L_B$ ratio) over the full $L_B$ range of the galaxy population. However, the sample used for this calculation contains both early and late types, which show different gas richness, because Ilbert et al. (2005) did not divide their sample into two galaxy types. Inclusion of early types in estimating the galaxy luminosity function changes the luminosity function shape, in particular making the faint end...
slope shallower (Loveday et al. 2012). Our correction for incomplete sampling of the luminosity function is sensitive to the slope at the faint end, where late-type galaxies with high $M_{B}/L_B$ are found. Applying too shallow a value for this slope means the correction does not add back in enough low-$L_B$ galaxies, and this means the final $\rho_{HI}$ may still be a little underestimated. Measuring separate luminosity functions for early- and late-type galaxies could give a more accurate correction.

As mentioned in many H I surveys and H I spectral stacking experiments (e.g. Zwaan et al. 1997, 2003, 2005; Rhee et al. 2013, 2016), H I self-absorption has not been accounted for in the $\rho_{HI}$ calculation because it is very difficult to assess to what extent H I self-absorption influences the H I mass and mass density estimation based on even the blind H I survey data (Zwaan et al. 2003, 2005). This is due to a lack of reliable measurements required to examine the effect, such as galaxy inclination measured in the optical bands. We assume that an underestimate of $\rho_{HI}$ caused by H I self-absorption (Zwaan et al. 1997) does not change the main result of this paper although Braun (2012) asserts the effect increases H I mass and density measurements by approximately 34 per cent. However, more data with high spectral and angular resolution are required to determine whether the assertion by Braun (2012), based on a small sample, is representative.

6.2 The Cosmic $H I$ Mass Density ($\Omega_{HI}$)

The $H I$ gas density ($\Omega_{HI}$) in units of the cosmic critical density is a useful parameter to express how the $H I$ gas content of galaxies evolves as a function of cosmic time (redshift). This is calculated as the comoving $H I$ gas density scaled by the critical density ($\rho_{HI}$) (e.g. Rhee et al. 2013, 2016). For the VVDS 14h field at $z \approx 0.32$, $\Omega_{HI} = (0.50 \pm 0.18) \times 10^{-3}$ as seen in Table 4 and Fig. 14. Other measurements shown in Fig. 14 were obtained using several different techniques: $H I$ emission from blind 21-cm emission surveys and H I spectral stacking at the lower redshifts (Zwaan et al. 2005; Lah et al. 2007; Martin et al. 2010; Freuding et al. 2011; Delhaize et al. 2013; Rhee et al. 2013; Hoppmann et al. 2015; Rhee et al. 2016); H I spectral stacking applied to star-forming galaxies at intermediate redshift ($z \approx 1.3$, Kanekar et al. 2016); a targeted survey of Mg II absorption systems and a blind DLA survey at intermediate redshifts (Rao et al. 2006, 2017; Neeleman et al. 2016); large DLA surveys at the higher redshifts (Prochaska et al. 2005; Noterdaeme et al. 2009, 2012; Zafar et al. 2013; Crighton et al. 2015; Bird et al. 2017). Our $\Omega_{HI}$ measurement agrees with the error bars with all of the measurements made at low redshifts, implying that there is little $H I$ gas evolution from $z \approx 0.4$ to present. Similarly, at $z > 2$ the $H I$ measurements based on large samples of DLAs are also fairly consistent with one another and indicate an increased $H I$ gas density at $z > 2$ as seen in Fig. 14.

Despite the agreement at low and high redshifts, measurements at $0.5 < z < 2.0$ are at odds with each other as well as very uncertain. This redshift regime is observationally challenging to both 21-cm and DLA techniques. At present, measurements in this range come predominantly from DLA studies and have large measurement uncertainties and discrepancies. The Lyman-$\alpha$ lines used to detect DLAs are still in the UV at these redshifts, which means that a space telescope with a UV spectograph is required. Furthermore, blind surveys for DLAs are inefficient because of the low surface density of DLAs at these redshifts. Given the limited observing time of $HST$ for UV spectroscopy, no large enough DLA surveys exist. In order to increase the efficiency of DLA observations, Rao et al. (2006) adopted pre-selection based on strong Mg II absorption, which most known DLAs have. Recently Neeleman et al. (2016) have compiled UV spectroscopic data from the $HST$ spectroscopic data archive accumulated over more than 20 years to conduct a blind DLA search. Although the number of DLAs that they identified is small (4 DLAs), their result is about four times lower in $\Omega_{HI}$, than that of Rao et al. (2006) with less uncertainty and is consistent with the lower-$z$ $\Omega_{HI}$ measurement from H I 21-cm observations. This discrepancy may be interpreted as a bias of the Mg II pre-selection method (a pre-selection cut of $W_{\lambda 2796} > 0.6$ Å, the rest-frame equivalent width of the Mg II 2796 Å) that Rao et al. (2006) used (Neeleman et al. 2016; Berg et al. 2017). However, Rao et al. (2017) recently provided an update of their previous Mg II pre-selection DLA survey, increasing their sample size from 41 to 70. They re-derived $\Omega_{HI}$ for a larger sample in the same redshift interval (0.11 < $z$ < 1.65). As seen in Fig. 14, their $\Omega_{HI}$ measurements are lower than their previous measurements, becoming closer to H I measurements at lower redshifts. They also claimed that their sample is statistically representative of the true DLA population at $z < 1.65$, denying claimed bias effects in their pre-selection method. Another upper limit on H I gas content was provided by Kanekar et al. (2016), who stacked 857 star-forming galaxies at $z = 1.265$ in the four DEEP2 fields. Their upper limit is consistent with that of Neeleman et al. (2016) but discrepant with the Rao et al. (2017) measurements. This redshift range has also been explored with a new observing technique called H I intensity mapping (Chang et al. 2010; Masui et al. 2013; Switzer et al. 2013). However these measurements are affected by systematics and bias factors that are poorly constrained, resulting in large uncertainty. To address the tension in this redshift range, instruments to conduct large blind surveys are likely required. As mentioned by Rao et al. (2017), there seems to be no plan for a large survey for DLA at $z < 1.65$ in the near future. However, forthcoming deep H I surveys using the SKA pathfinders will measure accurate $\Omega_{HI}$ at this redshift even before the SKA comes online (e.g. DINGO and LADUMA, Meyer 2009; Holwerda, Blyth & Baker 2012).

The most noticeable trend in Fig. 14 is that the DLA measurements at $z > 2$ consistently show a larger value of $\Omega_{HI}$ than the H I 21-cm emission measurements at $z < 0.4$. Unlike H I gas content measurement using 21-cm emission from galaxies, DLAs measure H I gas not only in galaxies but also around galaxies, for example H I streams and filaments. The observed difference may be pointing towards an increased contribution of neutral atomic gas outside galaxies at higher redshifts. Taking into account all $\Omega_{HI}$ measurements, the overall trend indicates $\Omega_{HI}$ at $z \sim 5$ is at least double the value in the local universe.

Theoretical understanding of the trends seen in Fig. 14 remains incomplete, and there are diverse results. While cosmological galaxy evolution simulations based on semi-analytic models (e.g. Lagos et al. 2014; Popping, Somerville & Trager 2014; Kim et al. 2015) are able to match the H I gas abundance observed at low redshifts, they have had difficulty reproducing the observed abundances at higher redshifts. For instance, Kim et al. (2015) predicted that $\Omega_{HI}$ shows little evolution at lower redshifts, well reproducing the trend of those H I observations, but decreases at $z > 2$, in conflict with the trend in Fig. 14. One reason for this tension could be that these authors modelled neutral gas only inside galaxies without attempting to estimate the neutral gas outside of galaxies, which is hard to model in their simulations. More recently, a cosmological hydrodynamic simulation called MUFASA (Dave et al. 2017) has yielded a good match to the observations (Fig. 14).
7 SUMMARY AND CONCLUSION

Stacking 21 cm H\textsc{i} measurements of 165 galaxies at $0.305 < z < 0.337$ shows that $\gtrsim 95$ per cent of the neutral gas is found in blue, star-forming galaxies. The average ratio of H\textsc{i} gas mass to blue luminosity in these galaxies (133 in our sample) is $\sim 0.5 \, M_\odot / L_\odot$. Among these late-type galaxies, those having lower stellar mass are more gas-rich than more massive ones. The cosmic H\textsc{i} gas density at $z = 0.32$ as a function of the cosmological critical density is $\Omega_{\text{HI}} = (0.50 \pm 0.18) \times 10^{-3}$. This value is in good agreement with results at $z = 0$ based on large-scale 21-cm surveys as well as other H\textsc{i} stacking measurements at $z < 0.4$. Our result at $z \approx 0.32$ plays a crucial role in supporting the previous result from Rhee et al. (2016) in the sense that all measurements of $\Omega_{\text{HI}}$ at $z < 0.4$ based on 21-cm line emission observations are consistent with no evolution in the neutral hydrogen gas density over the last $\sim 4$ Gyr. However the overall trend including DLA measurements at higher redshifts shows a factor of $\gtrsim 2$ higher $\Omega_{\text{HI}}$ at $z \sim 5$ than at the present epoch. Observations of H\textsc{i} at $z \gtrsim 0.5$ using upcoming radio telescopes will better define the evolution of $\Omega_{\text{HI}}$ between the local universe, where the gas is predominantly inside galaxies and higher redshifts.

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