The dynamical mass ejection from binary neutron star mergers: Radiation-hydrodynamics study in general relativity

Yuichiro Sekiguchi, Kenta Kiuchi, Koutarou Kyutoku, and Masaru Shibata

1Yukawa Institute for Theoretical Physics, Kyoto University, Kyoto, 606-8502, Japan
2Department of Physics, University of Wisconsin-Milwaukee, P.O. Box 413, Milwaukee, Wisconsin 53201, USA

(Dated: March 4, 2015)

We perform radiation-hydrodynamics simulations of binary neutron star mergers in numerical relativity on the Japanese "K" supercomputer, taking into account neutrino cooling and heating by an updated leakage-plus-transfer scheme for the first time. Neutron stars are modeled by three modern finite-temperature equations of state (EOS) developed by Hempel and his collaborators. We find that the properties of the dynamical ejecta of the merger such as total mass, average electron fraction, and thermal energy depend strongly on the EOS. Only for a soft EOS (the so-called SFHo), the ejecta mass exceeds 0.01M⊙. In this case, the distribution of the electron fraction of the ejecta becomes broad due to the shock heating during the merger. These properties are well-suited for the production of the solar-like r-process abundance. For the other stiff EOS (DD2 and TM1), for which a long-lived massive neutron star is formed after the merger, the ejecta mass is smaller than 0.01M⊙, although broad electron-fraction distributions are achieved by the positron capture and the neutrino heating.

PACS numbers: 04.25.D-, 04.30.-w, 04.40.Dg

I. INTRODUCTION

The merger of binary neutron stars (BNS) is one of the most promising sources of gravitational waves for advanced LIGO [1], advanced VIRGO [2], and KAGRA [3], which will start operation in a few years. The recent statistical studies suggest that these gravitational-wave detectors will observe gravitational waves from merger events as frequently as ~ 1–100/yr [4, 5]. The merger of BNS is also a promising candidate for the central engine of short-hard gamma-ray bursts. If gravitational waves are observed simultaneously with them, a long-standing puzzle on the central engine of short-hard gamma-ray bursts may be resolved.

In addition to these aspects, BNS are attracting attention as the nucleosynthesis site of heavy elements by the r-process [4], which may proceed in the neutrino-rich matter ejected during the merger. Recent observations of metal-poor stars [6] strongly suggest that there should exist 'main' r-stars affected by 'universal' r-process events in which the resulting abundance is close to that of solar-abundance pattern for nuclei with the atomic number Z ≥ 38 (A ≥ 90). It has recently been revealed [7, 8] that the supernova explosion, which was previously considered to be the most promising candidate for the site of the r-process, may not be a viable origin in this regard, and the BNS mergers is getting attention.

Furthermore, a strong electromagnetic emission may accompany the radioactive decay of the r-process elements [9, 10] and it could be an electromagnetic counterpart of gravitational waves from BNS mergers. An infrared transient event associated with GRB 130603B is the first candidate for such events [11]. These facts strongly encourage the community of gravitational-wave astronomy to explore the r-process nucleosynthesis and associated electromagnetic emission in the BNS merger.

For the quantitative study of these topics, we have to clarify the merger dynamics, subsequent mass ejection, and physical condition of the ejecta, which are necessary to study the nucleosynthesis, subsequent decay of the heavy elements in the ejecta, and electromagnetic emission from the ejecta. For this purpose, we have to perform BNS merger simulations taking into account both general relativistic gravity and detailed microphysical processes.

For the former, recent numerical relativity simulations (e.g., [12]; see also [13] for simulations in approximate general relativistic gravity) have clarified that the general relativistic gravity can be the key for the mass ejection: In general relativity, shock heating plays a prominent role in the merger process, and consequently, the ejecta that is dynamically expelled during the merger (dynamical ejecta) are composed not only of those driven by the tidal interactions but of those driven by the thermal pressure, by contrast with the result in Newtonian simulations (e.g., [14]) for which the tidal component is major.

For the latter, we have recently developed a neutrino-radiation hydrodynamics code, and now, we can perform simulations both employing a wide variety of equations of state (EOS) for the nuclear matter in which finite-temperature effects are incorporated and handling neutrino cooling and heating with reasonable sophistication.

This is the first study based on these modern aspects of the merger dynamics in general relativity taking into account the microphysics. In this paper, we report the latest result of our simulations for equal-mass BNS mergers of typical neutron-star mass (1.35M⊙) for three representative EOS, among which the radius of neutron stars is appreciably different. In this paper, we only consider
TABLE I. Characteristic properties of EOS at the nuclear saturation density. \(n_0\): the nuclear saturation density. \(E_0\): the binding energy. \(K\): the incompressibility. \(S\): the symmetry energy. \(L\): the logarithmic derivative of the symmetry energy.

| EOS     | \(n_0\) (fm\(^{-3}\)) | \(E_0\) (MeV) | \(K\) (MeV) | \(S\) (MeV) | \(L\) (MeV) |
|---------|----------------|--------------|-------------|-------------|------------|
| SFHo    | 0.1583         | 16.19        | 245.5       | 31.57       | 47.10      |
| DD2     | 0.1491         | 16.02        | 242.7       | 31.67       | 55.03      |
| TM1     | 0.145          | 16.3         | 281         | 36.9        | 110.8      |

the case of equal-mass binaries. The dependence on the mass-ratio and the total mass will be studied in a future work. We will show that the physical properties of the dynamical ejecta such as the mass and neutron fraction depend strongly on the EOS. We find that for producing mildly neutron-rich dynamical ejecta of large mass with a broad range of the electron fraction, a relatively soft EOS that yields small-radius (\(\lesssim 12\) km) neutron stars is necessary. Because of such a broad distribution of the electron fraction, the universal \([7]\) solar-abundance pattern of the \(r\)-process elements may be reproduced without need for the other contributions \([17]\).

II. METHOD, EOS, INITIAL MODELS, AND GRID SETUP

We solve Einstein’s equation by the puncture-BSSN (Baumgarte-Shapiro-Shibata-Nakamura) formalism as before \([13, 14]\). The 4th-order finite-differencing scheme is applied to discretize the field equations. The radiation hydrodynamics equations are solved by a recently-developed code which is updated from the previous version: In this new code, neutrino transport is computed in a leakage-based scheme \([20]\) incorporating Thorne’s moment formalism with a closure relation for a free-streaming component \([21]\). For neutrino heating, absorption on free nucleons is taken into account.

We employ three EOS for nuclear matter derived recently by Hempel and his collaborators, which are referred to as SFHo \([22]\), DD2 \([23]\), and TM1 \([24]\) in the following. TM1 EOS, which is also known as Shen EOS \([22]\), is based on the relativistic mean field theory with a parameter set of Ref. \([24]\) and have been used widely in both supernova and compact-binary merger simulations. SFHo EOS is constructed so that the predicted neutron star radius matches recent neutron star observations by extending the nonlinear Walecka model \([22]\). DD2 EOS is based on a relativistic mean field model with a density dependent coupling \([27]\). Some characteristic properties of EOS are listed in Table II.

For all of them, the predicted maximum mass for spherical neutron stars is larger than the largest well-measured mass of neutron stars, \(\approx 2M_\odot\) \([28]\). For these EOS, the radius of neutron stars with mass \(1.35M_\odot\) is \(R_{1.35} = 11.9\) km (SFHo), 13.2 km (DD2), 14.5 km (TM1), respectively (see Table II). We refer to an EOS with a small neutron star radius \((R_{1.35} \leq 12\) km\) like SFHo as a soft EOS and an EOS with a large radius \((R_{1.35} \geq 13\) km\) as a stiff EOS. The stellar radius plays a key role for determining the merger remnant and the properties of the dynamical ejecta.

In numerical simulations, we have to follow the ejecta with velocity \(0.1–0.3c\) (\(c\) is the speed of light), which expand to \(>10^4\) km in the simulation time. To follow the ejecta motion as well as to resolve neutron stars, we employ a fixed mesh-refinement algorithm. In this work, we prepare 9 refinement levels with the varying grid spacing \(\Delta x\) and the grid number \(N\). For each level, the computational domain covers \(35\) km in the simulation time. To follow the ejecta motion as well as to resolve neutron stars, we employ a fixed mesh-refinement algorithm. In this work, we prepare 9 refinement levels with the varying grid spacing \(\Delta x\) and the grid number \(N\). For each level, the computational domain covers \(35\) km in the simulation time. To check that the numerical results depend only weakly on the grid resolution, we also performed lower-resolution simulations. For this case, \(N = 160\) and \(\Delta x = 250\)–\(300\) m. As listed in Table II, we found that the results such as total ejecta mass and averaged values of \(Y_e\) depend very weakly on the grid resolution. Furthermore, to confirm the importance of the neutrino heating, we also performed simulations in which the neutrino absorption is switched off (denoted as ‘no-heat’ in Table II) and compared the results for the first time.

We consider equal-mass BNS with each mass \(1.35M_\odot\). Observed neutron stars in BNS typically have the mass ratio close to unity and the mass in the range \(1.20–1.45M_\odot\) \([29]\). Thus, our choice reasonably reflects the observational fact. The initial orbital separation is chosen so that the orbital angular velocity, \(\Omega\), satisfies \(Gm_0\Omega/c^3 = 0.028\) where \(m_0 = 2.7M_\odot\) is the sum of each mass in isolation and \(G\) gravitational constant, respectively. Table II lists the key parameters of our models.
$E_{\text{kin}}$ where $E_{\text{kin}}$ is kinetic energy of the ejecta. Figure 1 shows that the ejecta mass depends strongly on the EOS: For softer EOS (i.e., for smaller values of $R_{1.35}$), the ejecta mass is larger. Remarkable is that with the decrease of $R_{1.35}$ by $\sim 3$ km, the ejecta mass increases by more than one order of magnitude and only for $R_{1.35} \lesssim 12$ km the ejecta mass exceeds $0.01M_{\odot}$, as already indicated in [14, 15]. In the later phase, the total ejecta mass relaxes approximately to a constant, and the ejecta are in a free expansion phase for all the models.

There are two major mass ejection mechanisms during the merger phase. One is tidal interaction and the other is shock heating. By the tidal interaction, the matter tends to be ejected near the orbital plane. On the other hand, by the shock heating, the matter is ejected in a quasi-spherical manner. Because both effects play a role, the ejecta usually have a spheroidal morphology. For small values of $R_{1.35}$, the shock heating plays a stronger role and the ejecta in this case have a quasi-spherical morphology.

Figure 2 plots the profiles of the electron fraction, $Y_e$, (left half) and entropy per baryon, $s$, (right half) of the ejecta on the $x$-$y$ and $x$-$z$ planes for DD2 (left panel) and SFHo (middle and right panels). For DD2, the ejecta are composed of (i) tidally-ejected matter with low values of $Y_e$ and $s$ near the orbital plane and (ii) shock-heated matter with relatively high values of $Y_e$. The shock-heated ejecta are less neutron-rich because the temperature gets much higher than $\sim 1$ MeV as a result of the shock heating, producing copious $e^−e^+$ pairs that activate $e^−$ and $e^+$ captures by protons and neutrons, respectively. As a result of $e^−$ and $e^+$ captures, the luminosities of $\nu_e$ and $\bar{\nu}_e$ become quite high as $\gtrsim 10^{53}$ ergs/s (see Fig. 3), as long as the remnant MNS is present. Because the original ejecta are neutron-rich, $e^+$ capture dominates $e^−$ capture, and hence, the luminosity of $\bar{\nu}_e$ is higher than that of $\nu_e$ and the ejecta become less neutron-rich.

In addition to the tidal-driven and shock-heated components explained above, we found the third component in a later phase, that is, neutrino-heated component with even higher values of $Y_e$ and $s$ in the region above the MNS pole (see the high-entropy region in the left panel ($x$-$z$ plot) of Fig. 2). Furthermore, some fraction of the material obtains enough energy to be additional neutrino-driven ejecta. Possible existence of such a component was recently reported in a MNS system [32, 33] and a BH and torus system which is expected to be formed after the BNS mergers [34]. We confirmed the existence of the neutrino-driven component in self-consistent numerical-relativity simulations of the merger for the first time.

For TM1, the results are basically similar to those for DD2 except for the fact that the tidally-ejected component is more dominant and the $e^+$ capture is less efficient. Also, the neutrino-driven wind appears to play...
FIG. 2. Contours of the electron fraction, $Y_e$, (left half) and the entropy per baryon, $s$, (right half) in $x$-$y$ (lower) and $x$-$z$ (upper) planes. left panel: for DD2 at 8.5 ms after the merger. middle panel: for SFHo at 5.0 ms after the merger. right panel: for SFHo at 15.0 ms after the merger.

For SFHo, shock waves are formed for several times during the merger phase as the MNS oscillates with a high amplitude, and hence, a certain fraction of matter originally ejected by the tidal interaction is subsequently heated up by shocks ($s$ increases), resulting in the increase of the values of $Y_e$ via weak interactions. On the other hand, other parts less influenced by the shock heating preserve the neutron-rich nature of the original neutron stars. As a result of these two facts, the ejecta can have higher values of $s$ and $Y_e$ than for DD2 and TM1 even in the orbital plane with an appreciably inhomogeneous distribution of $Y_e$ (see the middle panel of Fig. 2). Because a BH is formed at $\sim 10$ ms after the onset of merger for SFHo, the strong neutrino emission region is swallowed into the BH and neutrino luminosity decreases to $\lesssim 10^{53}$ ergs/s. Hence, there is less clear neutrino-driven ejecta component for this EOS (see the bottom panel of Fig. 3).

The upper panel of Fig. 4 shows the time evolution of averaged values of $Y_e (\langle Y_e \rangle)$ from which the effect on $Y_e$ of the shock heating and the resulting positron capture can be seen more clearly. The several distinct changes in $\langle Y_e \rangle$ observed for SFHo in $\lesssim 5$ ms after the onset of merger reflect the strong $e^+$ capture activated by the shock heating. During this phase, $\langle Y_e \rangle$ for SFHo increases drastically to be $\approx 0.3$. After this phase, on the other hand, $\langle Y_e \rangle$ for SFHo is approximately constant because the $e^-$ and $e^+$ captures balances and because the neutrino luminosity decreases to be $\sim 10^{52}$ ergs/s due to the BH formation, which is not sufficient to change $\langle Y_e \rangle$ of the massive ejecta. Thus, for softer EOS like SFHo, $Y_e$ is likely to be increased primarily by the $e^+$ capture.

On the other hand, $\langle Y_e \rangle$ for DD2 and TM1 in the early stage is low as $Y_e \lesssim 0.1$--0.2, while it increases in time. This is simply because the shock heating at the first contact is not strong enough to increase $\langle Y_e \rangle$ significantly for these stiffer EOS; i.e., the original composition of the ejecta driven by tidal torque, which is composed primarily of neutron-rich matter with low temperature, is temporally preserved as found in [15, 16]. In the later phase, however, the ejecta become less neutron-rich. This is partly due to the positron capture discussed above. In addition, the electron neutrinos emitted from the remnant MNS convert some fraction of neutrons to protons via the electron neutrino capture (see below for a more
For stiffer EOS, the importance of the electron neutrino capture in increasing \(Y_e\) of the ejecta is enhanced because of their lower temperature and the maintained high neutrino luminosity from the long-lived MNS.

The lower panel of Fig. 4 plots the mass-distribution histograms for \(Y_e\) normalized by the total mass of the ejecta at \(\approx 25\) ms after the onset of merger. For all of the models, \(Y_e\) is distributed in a broad range between \(\sim 0.05\) and \(0.45\). This result is completely different from that found in the previous studies \([15, 16]\) in which the distribution of \(Y_e\) is very narrow with a lower average value \(\lesssim 0.1\). This disparity can be explained as follows.

In the previous approximate general relativistic study \([13]\), the weak interaction processes were not taken into account, and hence, the ejecta remain neutron-rich because there is no way to change \(Y_e\). In the previous Newtonian studies \([14]\), they took into account the neutrino cooling (\(e^-\) and \(e^+\) captures). However, as we mentioned already, the effect of the shock heating is underestimated significantly in Newtonian gravity, and hence, the effect of the \(e^+\) capture would be much weaker than that in our simulations due to the underestimated temperature. In addition, they did not take into account the neutrino heating (absorptions) which is expected to play a role for stiffer EOS in which the positron capture is relatively less important due to lower temperature.

To see the effects of the neutrino heating more quantitatively, we performed simulations without (no-heat) neutrino heating for SFHo and DD2. We found that for both EOS, the contribution of the neutrino-driven component in the ejecta mass is \(\sim 10^{-3} M_\odot\) at the end of the simulation (see Table I), which is consistent with that found in \([33]\). The amount of the neutrino-driven ejecta is minor for SFHo but comparable to the amount of the dynamical ejecta for DD2. This result suggests that the neutrino heating plays a relatively more important role for stiffer EOS like DD2 and TM1 in which the amount of the dynamical ejecta is \(\sim 10^{-3} M_\odot\).

The neutrino heating plays an important role in changing the chemical composition \(\langle Y_e \rangle\) of the ejecta. As shown in Fig. 8, the luminosities of \(\nu_e\) and \(\bar{\nu}_e\) are quite high as \(\gtrsim 10^{53}\) ergs/s. Due to the absorption of neutrinos with this high luminosity, the ejecta become more proton-rich because the electron neutrinos convert some fraction of neutrons to protons via the reactions \(n + \nu_e \leftrightarrow p + e^-\). Note again that \(\nu_e\) capture is more efficient than \(\bar{\nu}_e\) capture since the ejecta are neutron-rich.

Figure 5 compares the time evolution of \(\langle Y_e \rangle\) (upper panel) and the mass-distribution histograms for \(Y_e\) at \(\approx 25\) ms after the onset of merger (lower panel) between simulations with and without neutrino heating for SFHo and DD2. The results indicate that for SFHo, \(\langle Y_e \rangle\) is increased to be \(\approx 0.29\) due to the positron capture and the neutrino heating pushes it further by \(\approx 0.02\) at the end of the simulations. For DD2, the effect of the positron capture is weaker and the neutrino heating plays a relatively important role, increasing \(\langle Y_e \rangle\) by \(\approx 0.03\). Such enhancements of \(\langle Y_e \rangle\) due to the neutrino heating would be important in considering the \(r\)-process nucleosynthesis \([17]\).

The mass-distribution histograms also shift towards the higher \(Y_e\) side due to the neutrino heating. However, the distributions still show a broad feature even...
without the neutrino heating. This suggests that the positron capture resulting from the strong shock heating due to general relativistic gravity is primarily responsible for making the $Y_e$ distribution broad for DD2 and SFHo. For much stiffer EOS like TM1, the neutrino heating would play a relatively major role. Although our treatment for the neutrino transfer is an approximate one, our results indicate that the neutrino heating plays an important role in determining the chemical properties of the ejecta.

IV. SUMMARY AND DISCUSSION

We have reported the first numerical results of radiation hydrodynamics simulations in general relativity focusing on the properties of the dynamical ejecta of the equal-mass BNS merger with typical mass of each neutron star (1.35$M_\odot$). Three modern finite-temperature EOS are employed to clarify the dependence of the ejecta properties on the EOS. We found that the total mass of the ejecta is larger for softer EOS (giving smaller-radius neutron stars), and it exceeds 0.01$M_\odot$ only for the case that $R_{1.35} \lesssim 12$km, as indicated in [14]. As shown in [10, 12], the electromagnetic luminosity of the ejecta by the radioactive decay of the r-process elements would depend sensitively on the ejecta mass, and hence, the predicted range of the luminosity spans in a wide range due to the uncertainty of the nuclear-matter EOS.

We also found that the averaged value of $Y_e$ of the ejecta is higher for softer EOS like SFHo in which $R_{1.35}$ is smaller, reflecting the fact that the shock heating is more efficient. For all of the models, the value of $Y_e$ for the ejecta has a broad distribution between $\sim 0.1$ and 0.45, by contrast with the previous studies [15, 16]. Here, both the strong shock associated with general relativistic gravity and the weak interactions play crucial roles for this. Such a broad distribution may be well-suited for producing the universal solar-abundance pattern of r-process elements as illustrated in [17].

For the EOS but for SFHo, the dynamical ejecta mass is of order $10^{-3} M_\odot$. In this case, a rather higher merger rate of $\gtrsim 10^{-4} \text{ yr}^{-1}$ than the present estimates of the Galactic rate (a few $10^{-5} \text{ yr}^{-1}$) [35] is necessary to explain the amount of heavy r-process elements [36, 37], if the the dynamical ejecta from binary neutron star mergers is responsible for their production. In regards to this point, SFHo is an attractive EOS. We will study consequences of our results on the synthesis of heavy elements in the forthcoming paper. If EOS is not very soft like SFHo, some other contributions, such as mergers of black hole-neutron star binaries [38], disk winds from accretion torus around a merger remnant black hole [34, 39], and magnetorotational supernova explosions [40] may be necessary. In such cases, however, it is not clear whether the universality requirement can be achieved or not.

In this work, we focused only on the equal-mass binary case and did not explore the dependence of the results on the binary parameters such as the total mass and the mass ratio. As reported in [14], the relative importance of the tidal interactions and the shock heating in the dynamical mass ejection depends on the binary parameters. It is interesting to explore the dependence of the results on binary parameters for SFHo and the resulting abundance profile in the future work, because the observed abundance patterns of the metal-poor, r-rich stars show some diversity in the lower mass-number region [7]. Also, we did not continue our simulations beyond 30–40 ms after the onset of merger. For the longer time scales, magnetohydrodynamic processes [41], viscous heating, and nuclear recombination [42] could be important. Self-consistent studies of these effects in the BNS merger also have to be done in the future.

ACKNOWLEDGMENTS

We are grateful to M. Hempel for providing the EOS table data and S. Wanajo for discussions. Numerical computations were performed on the supercomputer K at AICS, XC30 at CICA of NAOJ, FX10 at Information Technology Center of Tokyo University, and SR16000 at YITP of Kyoto University. This work was supported by Grant-in-Aid for Scientific Research (24244028, 24740163, 25103510, 25105508), for Scientific Research on Innovative Area (24103001), by HPCI Strategic Program of Japanese MEXT/JSPS (Project No. hpci130025, 140211). Koutarou Kyutoku is supported by JSPS Postdoctoral Fellowship for Research Abroad.
