Evidence for $X(3872) \rightarrow J/\psi \pi^+ \pi^-$ produced in single-tag
two-photon interactions

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Abstract

We report the first evidence for $X(3872)$ production in two-photon interactions by tagging either the electron or the positron in the final state, exploring the highly virtual photon region. The search is performed in $e^+e^- \rightarrow e^+e^- J/\psi\pi^+\pi^-$, using 825 fb$^{-1}$ of data collected by the Belle detector operated at the KEKB $e^+e^-$ collider. We observe three $X(3872)$ candidates with an expected background of $0.11 \pm 0.10$ events, with a significance of $3.2\sigma$. We obtain an estimated value for $\tilde{\Gamma}_{\gamma\gamma}B(X(3872) \rightarrow J/\psi\pi^+\pi^-)$ assuming the $Q^2$ dependence predicted by a $c\bar{c}$ meson model, where $-Q^2$ is the invariant mass-squared of the virtual photon. No $X(3915) \rightarrow J/\psi\pi^+\pi^-$ candidates are found.

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The charmonium-like state $X(3872)$ has been observed in various reactions since its first observation in $B \rightarrow KJ/\psi\pi^+\pi^-$ decays [1]. Its spin, parity, and charge conjugation were determined to be $1^{++}$ [2], but its internal structure is still a puzzle [3, 4]. Subsequent to the spin-parity determination, the $X(3872)$ has not been searched for in two-photon interactions because axial-vector particles are forbidden to decay to two real photons [5]. However, it has been pointed out that mesons with $J^{PC} = 1^{++}$ could be produced if one or both photons are highly virtual [6]—denoted as $\gamma^*$. We have performed the first search for the production of the $X(3872)$ by two photons, using $e^+e^- \rightarrow e^+e^- X(3872)$, where one of the final-state electrons, referred to as a tagging electron, is observed, and the other scatters at an extremely forward (backward) angle and is not detected [7]. Such events are called single-tag events. The $X(3872)$ is reconstructed via its decay to $J/\psi\pi^+\pi^- (J/\psi \rightarrow \ell^+\ell^-)$. The two-photon decay width, which is obtained from this measurement, is sensitive to the internal structure of the $X(3872)$. Early attempts to calculate such decay widths for charmonium-like exotic states have been reported in Ref. [8]. The measurement reported here gives new insight to the $X(3872)$ puzzle. We also search for the $X(3915)$ in the same final state, $J/\psi\pi^+\pi^-$, through the $G$-parity-violating $J/\psi\rho^0 (\rho^0 \rightarrow \pi^+\pi^-)$ channel, as well as $J/\psi\omega (\omega \rightarrow \pi^+\pi^-)$ decay[9].

We use 825 fb$^{-1}$ of data collected by the Belle detector operated at the KEKB $e^+e^-$ asymmetric collider [10, 11]. The data were taken at the $\Upsilon(nS)$ resonances ($n \leq 5$) and nearby energies, $9.43 \text{ GeV} < \sqrt{s} < 11.03 \text{ GeV}$. Of these data, 636 fb$^{-1}$ are at, or 60 MeV
below, the $\Upsilon(4S)$ resonance.

The Belle detector is a general-purpose magnetic spectrometer, asymmetrically enclosing the $e^+e^-$ interaction point [12, 13]. Charged-particle momenta are measured by a silicon vertex detector and a cylindrical drift chamber. Electron and charged-pion identification relies on a combination of the drift chamber, time-of-flight scintillation counters, aerogel Cherenkov counters, and an electromagnetic calorimeter made of CsI(Tl) crystals. Muon identification relies on the drift chamber and 14 layers of resistive plate chambers in the iron return yoke.

For Monte Carlo (MC) simulations, used to set selection criteria and derive the reconstruction efficiency, we use TREPSBSS [14, 15] to generate single-tag $e^+e^- \rightarrow e^+e^-X(3872)$ events in which the $X(3872)$ decays to $J/\psi \pi^+\pi^-$ and $J/\psi$ decays leptonically. For simulating radiative $J/\psi$ decays, we use PHOTOS [16, 17]. A GEANT3-based program simulates the detector response to these events [18].

Since one final-state electron is not detected, we select events with exactly five charged tracks, each coming from the interaction point (IP) and having $p_T > 0.1$ GeV/c, with two or more having $p_T > 0.4$ GeV/c, where $p_T$ is the transverse momentum with respect to the $e^+$ direction.

$J/\psi$ candidates are reconstructed by their decays to $e^+e^-$ or $\mu^+\mu^-$ pairs. A charged track is identified as an electron (muon) from the $J/\psi$ decay if its electron (muon) likelihood ratio is greater than 0.66 [19, 20][21] The invariant mass of the lepton pair is required to be in the range 3.047–3.147 GeV/$c^2$. In the calculation of the invariant mass of an $e^+e^-$ pair, we include the four-momenta of radiated photons, having energy less than 0.2 GeV and angle relative to an electron direction of less than 0.04 radians.

The tagging electron must have an electron likelihood ratio greater than 0.95 or $E/p$ greater than 0.87, where $E$ is the energy measured by the electromagnetic calorimeter and $p$ is the momentum of the particle. We require that the tagging electron have momentum above 1 GeV/c and $p_T > 0.4$ GeV/c. The electron momentum includes the momenta of radiated photons, using the same requirements as for the electrons from $J/\psi$ decays.

We identify a charged track as a pion if its kaon likelihood ratio is less than 0.8, its muon likelihood ratio is less than 0.9, its electron likelihood ratio is less than 0.6, and its $E/p$ is less than 0.8 [22]. We require that events do not have any photons with energy above 0.4 GeV or any $\pi^0$ candidates whose $\chi^2$ value in the mass constrained fit is less than 4.0.
As the $X(3872)$ should be back-to-back with the tagging electron projected in the plane perpendicular to the $e^+e^-$ beam axis, we require the difference between their azimuthal angles be in the range $(\pi \pm 0.1)$ radians.

We require that the total visible transverse momentum of the event, $p_T^*$ [23], be less than 0.2 GeV/c. We also require that the measured energy of the $J/\psi \pi^+ \pi^-$ system, $E_{\text{obs}}^*$, be consistent with the expectation, $E_{\text{exp}}^*$, calculated from the observed momentum of the tagging electron and the direction and invariant mass of the $J/\psi \pi^+ \pi^-$ system, imposing energy-momentum conservation. Since the energy and total transverse momentum are correlated, we impose a two-dimensional selection criterion

$$(p_T^* + 40 \text{ MeV}/c) \left( \frac{|E_{\text{obs}}^* - E_{\text{exp}}^*|}{E_{\text{exp}}^*} + 0.003 \right) < 3 \text{ MeV}/c.$$

(1)

Figure 1 shows the distribution of events and these selection criteria in the $p_T^*$ vs. $E_{\text{obs}}^*/E_{\text{exp}}^*$ plane.

FIG. 1. $p_T^*$ vs. $E_{\text{obs}}^*/E_{\text{exp}}^*$ distribution from data. The (red) line shows the selection criteria applied to $p_T^*$ and $E_{\text{obs}}^*/E_{\text{exp}}^*$; events below the line are accepted.

Finally, we place a requirement on the missing momentum of the event, which is equal to the momentum of the unmeasured electron that goes down the beam pipe. We require the missing-momentum projection in the $e^-$ beam direction in the center-of-mass frame be less than $-0.4$ GeV/c for $e^-$-tagging events and greater than 0.4 GeV/c for $e^+$-tagging events.

We search for the $X(3872)$ and $X(3915)$ by looking for events in the $J/\psi \pi^+ \pi^-$ invariant mass distribution, $M(J/\psi \pi^+ \pi^-)$. The reconstructed mass resolution is expected to be 2.5 MeV/$c^2$ from the MC simulation. We define two signal regions: 3.867–3.877 GeV/$c^2$
for the $X(3872)$ and 3.895–3.935 GeV/$c^2$ for the $X(3915)$. The former accommodates the $X(3872)$ with the known mass of $3871.69 \pm 0.17$ MeV/$c^2$ and the small decay width of less than 1.2 MeV [24]; the latter accommodates the $X(3915)$ with the known mass of $3918.4 \pm 1.9$ MeV/$c^2$ and the larger decay width of $20 \pm 5$ MeV. We constrain the $J/\psi$ mass to 3.09690 GeV/$c^2$ when we calculate $M(J/\psi\pi^+\pi^-)$ [25].

The dominant background, centered at 3.686 GeV/$c^2$, arises from radiatively produced $\psi(2S)$, $e^+e^- \rightarrow e^+e^-\psi(2S)$, with $\psi(2S) \rightarrow J/\psi\pi^+\pi^-$. Figure 2 shows the $M(J/\psi\pi^+\pi^-)$ distribution in data in the vicinity of $\psi(2S)$. Although the width of the $\psi(2S)$ peak is 2.7 MeV/$c^2$, its tail extends to the high-mass side. This feature was also seen in previous studies of initial-state-radiation (ISR) production of $J/\psi\pi^+\pi^-$ [26]. To remove $\psi(2S)$ events, we veto events within 0.03 GeV/$c^2$ of the $\psi(2S)$ mass, 3.686 GeV/$c^2$. Figure 3 shows the $Q^2$ distribution after removing those events, where $Q^2 = 2(p_{\text{in}} \cdot p_{\text{out}} - m_e^2 c^2)$ with $p_{\text{in}}$ and $p_{\text{out}}$ being the four-momenta of the incoming (beam) and outgoing (tagging) electrons and $m_e$ being the electron mass. In Fig. 3, data are dominated by background events while MC is pure $X(3872)$. Since two-photon processes are strongly suppressed at high $Q^2$, we require $Q^2 < 25$ GeV$^2$/c$^2$ to suppress non-two-photon background. Our measurement is insensitive for $Q^2 < 1.5$ GeV$^2$/c$^2$ due to a drop in reconstruction efficiency.

Figure 4 shows the observed events in the $Q^2$ vs. $M(J/\psi\pi^+\pi^-)$ plane. Three events are in the $X(3872)$ signal region; no events are in the $X(3915)$ region. The masses of the three events in the $X(3872)$ signal region are 3.8726, 3.8701 and 3.8742 GeV/$c^2$, giving the

FIG. 2. $M(J/\psi\pi^+\pi^-)$ distribution shown with the $\psi(2S)$ veto (shaded gray region).
FIG. 3. $Q^2$ distribution for data (blue dots) and MC (red histogram). The area of MC distribution is normalized to that of data. The vertical (magenta) line indicates the applied selection requirement.

The averaged mass of 3.8723±0.0012 GeV/$c^2$, where the uncertainty is statistical. At masses below the $X(3872)$ region, 3.716-3.867 GeV/$c^2$, there are six events, presumably from \( \psi(2S) \) events; at masses above, there are no events below 4.266 GeV/$c^2$, in region of the $Y(4260)$ mass. A similar distribution was seen in the Belle ISR study [26], suggesting that the main cause of our background is $t$-channel photon-exchange processes with an emission of a single virtual photon that converts to the hadronic state.

FIG. 4. Observed events (red dots) in the $Q^2$ vs. $M(J/\psi \pi^+ \pi^-)$ plane. Three events are seen in the $X(3872)$ signal region (red lines with shade). The blue lines with shade show the $X(3915)$ signal region. The vetoed regions are shaded gray with dash lines.

To estimate the background level in the $X(3872)$ signal region, we fit a linear function

$$\max(0, a[M(J/\psi \pi^+ \pi^-) - 3.872 \text{ GeV}/c^2] + b)$$  

(2)
to the data in the mass region of ±0.156 GeV/c² centered at the mass of the X(3872), excluding the signal region; a and b are free parameters of the fit. The width of 0.156 GeV/c² is determined by the distance between the X(3872) and the upper boundary, 3.716 GeV/c², of the ψ(2S) vetoed region. Using an unbinned extended maximum-likelihood fit, we obtain \(a = -345 \pm 195/(\text{GeV/c}^2)^2\) and \(b = 10.5 \pm 10.1/(\text{GeV/c}^2)\). This gives 0.11 ± 0.10 background events in the X(3872) signal region, where the uncertainty is statistical only. By comparing this result to that from the power function, \(a'/[M(J/ψ\pi^+\pi^-) - b']\), with \(b'\) fixed at 2.4 GeV/c², we estimate the systematic uncertainty to be ±0.01 events. Combining the statistical and systematic uncertainties in quadrature, we estimate 0.11 ± 0.10 background events.

With this background, the significance of three events is 3.2σ. For the X(3872) signal, with three observed and 0.11 expected background events, we calculate the number of signal events, \(N_{\text{sig}} = 2.9^{+2.2}_{-2.0}\) (stat.) ± 0.1 (syst.), using the Feldman-Cousins method [27] at 68% confidence level (C.L.). For the X(3915) signal, with zero observed and 0.3 expected background events, \(N_{\text{sig}} < 2.14\) at 90% C.L.

The differential cross section for the production of a resonance (X) in a single-tag two-photon interaction is expressed as [28]

\[
\frac{d\sigma_{ee}(X)}{dQ^2} = 4\pi^2 \left(1 + \frac{Q^2}{M^2}\right) \frac{2J + 1}{M^2} \Gamma_{\gamma^*\gamma}(Q^2)
\]

\[
\times 2 \frac{d^2L_{\gamma^*\gamma}}{dWdQ^2}\bigg|_{W=M},
\]

where \(L_{\gamma^*\gamma}\) is the single-tag luminosity function, \(M\) is the resonance mass, \(-Q^2\) is the invariant mass squared of the virtual photon, \(\Gamma_{\gamma^*\gamma}(Q^2)\) is the \(\gamma^*\gamma\) decay width for the resonance, \(W\) is the invariant mass of the \(\gamma^*\gamma\) system, and \(J\) is the resonance spin. The factor of two comes from the existence of two production modes: \(e^-\gamma^*\) and \(e^+\gamma^*\) scattering.

For a \(J=1\) resonance, spin-parity conservation forbids production at \(Q^2 = 0\). To remove the \(Q^2\)-dependence from \(\Gamma_{\gamma^*\gamma}(Q^2)\), we use the reduced \(\gamma\gamma\) decay width \(\tilde{\Gamma}_{\gamma\gamma}\) defined as [6, 29]

\[
\tilde{\Gamma}_{\gamma\gamma} \equiv \lim_{Q^2 \to 0} \frac{M^2}{Q^2} \Gamma_{\gamma^*\gamma}^{LT}(Q^2),
\]

using its \(Q^2\) dependence near zero; \(\Gamma_{\gamma^*\gamma}^{LT}\) is the \(\gamma^*\gamma\) decay width corresponding to a formation of the resonance from a longitudinal (virtual) photon and a transverse (real) photon. By substituting this expression into Eq. (3), we obtain

\[
\frac{d\sigma_{ee}(X)}{dQ^2} = 4\pi^2 \frac{3}{M^2} \frac{Q^2}{M^2} \tilde{\Gamma}_{\gamma\gamma} \frac{d^2L_{\gamma^*\gamma}}{dWdQ^2}\bigg|_{W=M},
\]

(5)
for $Q^2 \ll M^2$, where an extra factor of two comes from the difference in the number of spin degrees of freedom: the longitudinal component has one degree of freedom and the transverse component has two degrees of freedom in unpolarized incident photons. The quantity $\epsilon$ in Eq. (5) is the ratio $L_{LT}/L_{TT}$, where $L_{LT}$ is the luminosity function for the production of one longitudinally polarized photon and one transversely polarized photon and $L_{TT}$ is that of two transversely polarized photons. Using the Schuler-Berends-Gulik (SBG) model \cite{30} for $q\bar{q}$-type axial-vector mesons, this can be extended to a higher $Q^2$ region \cite{29} as

$$\frac{d\sigma_{ee}(X)}{dQ^2} = \tilde{\Gamma}_{\gamma\gamma} F(M, Q^2, \epsilon) \frac{d^2L_{\gamma^*\gamma}}{dWdQ^2} \bigg|_{W=M},$$

(6)

where

$$F(M, Q^2, \epsilon) = \frac{48\pi^2}{M^2} \frac{Q^2}{2M^2} + \epsilon \frac{Q^2}{M^2} \left(1 + \frac{Q^2}{M^2}\right)^3,$$

(7)

accounting for the contributions from helicity 0 and 1.

To obtain the relation between the number of signal events and the decay width, $\tilde{\Gamma}_{\gamma\gamma}$, we use Eqs. (6) and (7) assuming the $X(3872)$ is a pure $c\bar{c}$ state \cite{6}

$$N_{\text{sig}} = L_{\text{int}} B(X \to J/\psi \pi^+ \pi^-) B(J/\psi \to \ell^+ \ell^-) \times \tilde{\Gamma}_{\gamma\gamma} \int_{Q^2_{\text{min}}}^{Q^2_{\text{max}}} dQ^2 F(M, Q^2, \epsilon) \epsilon_{\text{eff}}(Q^2) \frac{d^2L_{\gamma^*\gamma}}{dWdQ^2} \bigg|_{W=M},$$

(8)

where $\epsilon_{\text{eff}}(Q^2)$ is the $Q^2$-dependent reconstruction efficiency, $L_{\text{int}}$ is the integrated luminosity, $B(X \to J/\psi \pi^+ \pi^-)$ is the branching fraction of the $X(3872)$ to $J/\psi \pi^+ \pi^-$, and $B(J/\psi \to \ell^+ \ell^-) = 0.1193$ is the branching fraction of $J/\psi$ to lepton pairs \cite{25}. We estimate the reconstruction efficiency from MC, in which we model the $X(3872)$ decay as $X(3872) \to J/\psi \rho^0$ with $J/\psi \to \ell^+ \ell^-$ and $\rho^0 \to \pi^+ \pi^-$ and with all daughter particles isotropically distributed in the rest frames of their parents. The decay model via $\rho$ is motivated by the measured invariant mass distributions \cite{1, 31, 32}. It has a reconstruction efficiency 12% higher than that of non-resonantly produced $\pi^+ \pi^-$; we include a 6% systematic uncertainty to account for this. The angular distribution of the decay products of the $X(3872)$ negligibly affects the reconstruction, as confirmed by simulating with an alternative model with decay angles of daughters from a $J^P = 1^+$ resonance with helicities 0 and 1. We estimate the efficiencies for our three center-of-mass beam energies—5.01, 5.29 and 5.43 GeV, corresponding to the $\Upsilon(2S)$, $\Upsilon(4S)$, and $\Upsilon(5S)$ resonance energies—and average the values weighted by their corresponding integrated luminosities. We also average over
the four detection modes given the two tagging charges \((e^+ \text{ and } e^-)\) and the two \(J/\psi\) decay modes \((e^+e^- \text{ and } \mu^+\mu^-)\). Figure 5 shows the result.

![Graph showing beam-energy-averaged reconstruction efficiency, \(\varepsilon_{\text{eff}}\), as a function of \(Q^2\). Each data point has 13% systematic uncertainty.](image)

FIG. 5. Beam-energy-averaged reconstruction efficiency, \(\varepsilon_{\text{eff}}\), as a function of \(Q^2\). Each data point has 13% systematic uncertainty.

The luminosity functions for our three beam energies are calculated as functions of \(Q^2\) using TREPSBSS. We set \(\epsilon = 1\) as a convention for the present application of Eq. (7)[6]. After performing the \(Q^2\) integration in Eq. (8), from \(Q_{\text{min}}^2 = 1.5 \text{ GeV}^2/c^2\) to \(Q_{\text{max}}^2 = 25 \text{ GeV}^2/c^2\), we obtain

\[
\tilde{\Gamma}_{\gamma\gamma} \mathcal{B}(X(3872) \to J/\psi \pi^+\pi^-) = (1.88 \pm 0.24) \text{ eV} \times N_{\text{sig}},
\]

including the total systematic uncertainty from the integration.

The dominant systematic uncertainty on the product \(\tilde{\Gamma}_{\gamma\gamma} \mathcal{B}(X \to J/\psi \pi^+\pi^-)\) is that on the reconstruction efficiency, primarily due to the differences between MC and data shown in Table I as effects due to selection criteria. The \(e^+e^-\) background uncertainty in the \(J/\psi\) selection, 7%, comes from the difference between MC and data in the \(e^+e^-\) background level. We estimate that the total systematic uncertainty is 13%.

From \(N_{\text{sig}}\), we determine

\[
\tilde{\Gamma}_{\gamma\gamma} \mathcal{B}(X \to J/\psi \pi^+\pi^-) = 5.5^{+1.1}_{-3.8} \text{ (stat.)} \pm 0.7 \text{ (syst.) eV}.
\]

To place a limit on \(\tilde{\Gamma}_{\gamma\gamma}\), we need \(\mathcal{B}(X \to J/\psi \pi^+\pi^-)\). We derive an upper limit, using the measured products of \(B\)-meson decay branching fractions and the \(X(3872)\) decay branching fractions, \(\mathcal{B}(B^+ \to K^+X)\mathcal{B}(X \to J/\psi \pi^+\pi^-\text{ and other specific final states})\) [33]. With the measured lower limit [25, 31, 34], this gives \(0.032 < \mathcal{B}(X \to J/\psi \pi^+\pi^-) < 0.061\) at the 90% C.L. Using the Feldman-Cousins method for three observed events and 0.11 background, we obtain \(0.995 < N_{\text{sig}} < 7.315\) at the 90% C.L. This, with Eq. (9), divided by \(\mathcal{B}(X \to\)
J/ψπ⁺π⁻), gives the range: 20-500 eV. This range is consistent with values predicted for the c̅c model [6, 8]. For non-c̅c models, we have to wait for improved calculations in the future.

| Item               | Subitem                                      | Uncertainty | Total |
|--------------------|----------------------------------------------|-------------|-------|
| J/ψ                | Electron and muon ID selections              | 4%          |       |
|                    | e⁺e⁻ background                              | 7%          |       |
|                    | J/ψ mass selection                           | 1%          |       |
|                    | Subtotal                                     | 8%          |       |
| Tag                | Electron ID selection                        | 3%          |       |
|                    | γ radiation from e±                           | ~0%         |       |
|                    | p criterion                                  | 4%          |       |
|                    | p_T criterion                                | 1%          |       |
|                    | Fake tag                                     | 0.3%        |       |
|                    | Subtotal                                     | 5%          |       |
| M(π⁺π⁻) MC model in X(3872) decay |                             | 6%          |       |
| Pion ID selections |                                             | 3%          |       |
| p_T-E_{obs}/E_{exp} selection |                         | 4%          |       |
| p_T criterion      |                                             | 1%          |       |
| Missing p criterion|                                             | 2%          |       |
| Back-to-back selection |                                         | 2%          |       |
| Track finding      |                                             | 1.4%        |       |
| MC data size       |                                             | 0.6%        |       |
|                    | Subtotal for efficiency systematics          | 13%         |       |
| Q² integration     |                                             | 1%          |       |
| Luminosity measure |                                             | 1.4%        |       |
| Luminosity function|                                             | 3%          |       |
| B(J/ψ → ℓ⁺ℓ⁻)      |                                             | 0.4%        |       |
|                    | Total                                        | 13%         |       |
No events consistent with $X(3915) \rightarrow J/\psi\pi^+\pi^-$ are observed. This, combined with the past measurements [9, 35], indicates there is no excess of $G$-parity-violating decays of $X(3915)$.

In summary, we find the first evidence for $X(3872)$ production in two-photon, $\gamma^*\gamma$, interactions. We observe three $X(3872)$ candidates with a significance of $3.2\sigma$ and an estimated yield of $2.9^{+2.2}_{-2.0}$ (stat.) ± 0.1 (syst.). From this, we obtain $\Gamma_{\gamma\gamma} \mathcal{B}(X(3872) \rightarrow J/\psi\pi^+\pi^-) = 5.5^{+4.1}_{-3.8}$ (stat.) ± 0.7 (syst.) eV, using the $Q^2$ dependence expected from a $c\bar{c}$ meson model. With future advances in the calculations of $\Gamma_{\gamma\gamma}$ for non-$c\bar{c}$ states and the higher luminosities of Belle II, it is expected that this method will contribute to the clarification of the nature of the $X(3872)$.

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