Nucleosynthesis of heavy elements in gamma ray bursts

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The ultrarelativistic jets responsible for prompt and afterglow emission in gamma ray bursts are presumably driven by a central engine that consists of a dense accretion disk around a spinning black hole. We consider such engine, composed of free nucleons, electron-positron pairs, Helium nuclei, and cooled by neutrino emission. A significant number density of neutrons in the disk provide conditions for neutron rich plasma in the outflows and jets. Heavy nuclei are also formed in the accretion flow, at the distances 150-250 gravitational radii from the black hole. We study the process of nucleosynthesis in the GRB engine, depending on its physical properties. Our results may have important observational implications for the jet deceleration process and heavy elements observed in the spectra of GRB afterglows.

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1. Introduction

Gamma ray bursts observed by Swift satellite reach the distances up to redshift of about 8 (e.g. GRB 090423, z=8.3). Many of the long duration GRBs, statistically more frequently detected than short ones, are observationally associated with supernovae (e.g. GRB 130427A). This fact supports the idea that had been put forward more than 20 years ago (Narayan, Paczynski & Piran, 1992) about gamma ray bursts being the signatures of death throes of massive stars. This progenitor star, while it is collapsing and forming a black hole in its center, supports the production of ultra-relativistic jets, which are ultimately responsible for the observed transient gamma ray emission. Due to the extremely large rate of accretion onto the central black hole, in this kind of engine, so called 'collapsar', we should encounter a rotationally supported transient disk with huge, nuclear densities and temperatures reaching $kT \sim 1\text{MeV}$. These conditions are therefore sufficient for production of heavy elements in the body of accretion disk, whose mass is about several solar masses (Popham et al. 1999).

In the case of short duration GRBs, the situation is somewhat more difficult to probe, because of the poor statistics. Only about 20 of GRBs with durations less than 2 seconds, have the measurements of their spectroscopic redshifts, and have been localized in their host galaxies. Also, the mergers of two neutron stars, which are frequently invoked as progenitors of short GRBs, may result in the formation of a $\sim 2.5 - 3M_\odot$ black hole, surrounded by a disk with a mass of only 0.2-0.5 solar masses (Ruffert & Janka 1998; Kluzniak & Lee 1998). Thus, even though the accretion rate is even higher than in case of long GRBs and nuclear matter densities are reached, the amount of distinct heavy element species might be too small to be detectable.

2. Accretion disk in the GRB central engine

The collapsar interpretation of long-duration gamma ray bursts invokes the existence of a rotating disk, or torus, in the interior of a collapsing star, fed by an external reservoir of stellar matter due to the fallback after supernova explosion. In the case of short duration GRBs, such torus should also have been formed, from the matter left by a disrupted compact star, albeit the duration of the accretion phase is limited. In general, accretion disks in the context of gamma ray bursts are expected to have typical densities of $10^{10-12} \text{g cm}^{-3}$, and temperatures that exceed $10^{11} \text{K}$ in the innermost $\sim 20$ Schwarzschild radii from the newly formed black hole. The accretion proceeds with rates up to several Solar mass per second. In this hyper-accreting regime, the photons are completely trapped in matter and are not efficient at cooling the disk. However, in the weak interactions, neutrinos are produced and thus provide a mechanism for cooling the flow. Moreover, at high accretion rates such torus becomes geometrically 'slim', with $H/r \sim 0.5$, and the advection of energy provides the cooling mechanism that is more efficient than neutrino emission.

To compute the structure of accretion disk, we need to take carefully into account the equation of state of its plasma. In the physical conditions implied by hyper-accretion, the plasma equation of state will be very different from an ideal gas, and now also the pressure of degenerate species, mainly electrons and positrons, as well as due to radiation and neutrinos, will contribute to EOS. We determine the EOS of the disk numerically, including the appropriate Fermi-Dirac statistics for the nuclear pressure of free neutrons, protons, and electron-positron pairs. We also take into
Figure 1: Physical conditions in the torus accreting in the GRB central engine and its outflows. The maps show temperature (left panel) and density with overplotted velocity field (right panel), in the innermost 50 $r_g$ around the black hole. Parameters: black hole mass $M = 10 M_\odot$, spin $a = 0.9$, mass of the disk $M_d = 1.0 M_\odot$. Snapshot is taken from axisymmetric GR MHD simulation at time $t = 0.0296$ s.

We studied the properties of accretion torus in GRB central engine with both 1-dimensional (vertically integrated), stationary, simplified models, using the assumption of a classical Shakura-Sunyaev $\alpha$-viscosity prescription, as well as with the 2-dimensional, time-dependent GR MHD computations, where the viscosity is provided by the magneto-rotational turbulence. The results were presented already in a series of articles, and the recent work (Janiuk et al. 2013) has shown that the resulting density and temperature distributions, as well as the neutrino emissivities, have very similar profiles, at least within the distance of the inner $\sim 50 r_g$ from the black hole.

As was estimated by Surman & McLaughlin (2004), the electron fraction in the outflowing material may be changed by 10-60%, for an assumed constant velocity. Later on, these authors (Surman et al. 2011) showed that production of nickel depends sensitively on the entropy in the outflowing material. The outflows velocity was assumed there to have a simple power-law dependence with distance, and a fixed starting position. To determine accurately the mass fractions...
of heavy elements, we need in fact to model both the chemical composition and evolution of the structure of the flow with magnetic turbulence, in order to accurately describe the flow properties.

3. Statistical Reaction Network

To compute the abundances of heavy elements, we use the thermonuclear reaction network code (http://webnucleo.org). The computational methods are described in detail in the literature (e.g., Wallerstein et al. 1997).

In a nutshell, the nuclear transmutations of subsequent species are tracked via the rate equations of the form:

\[ \dot{Y}_i = \sum_j N_{j,i} \lambda_j Y_j + \sum_{j,k} N_{j,k,l} \rho (\mathcal{A}_l)^2 < j,k,l > Y_j Y_k - Y_j Y_l \]  \hspace{1cm} (3.1)

where \( Y_i = n_i / \rho \mathcal{A}_i \) is the abundance of the \( i \)-th isotope, with \( \mathcal{A}_i \) being the Avogadro number, \( \lambda_j \) is the decay rate of the \( j \)-th isotope, and the last two terms represent the encounters of 2 or 3 reactant nuclei. Such a formulation allows for a separation of the nuclear changes in plasma composition from the hydrodynamical effects. For the nuclei of atomic weight \( A_i \), the condition \( \sum A_i Y_i = 1 \) is satisfied. The charge conservation condition must also be satisfied, so \( \sum Z_i Y_i = Y_e \) holds, under a given electron fraction \( Y_e \). The integrated cross-sections for interactions between target \( j \) and projectile \( k \) is expressed as:

\[ < j,k >= \sigma v >_{j,k} = \left( \frac{8}{\mu \pi} \right)^{1/2} (k_B T)^{-3/2} \int_0^{\infty} E \sigma(E) \exp(-E/k_B T) dE \]  \hspace{1cm} (3.2)

where \( \mu \) is the reduced mass of the target-projectile system, \( E \) is the center of mass energy, \( T \) is the temperature, and \( k_B \) is the Boltzmann constant.

For nuclei, in general the Maxwell-Boltzmann statistics applies, while for the photodisintegration cross-section photons must obey the Planck statistics. Note, however, that since the photodisintegration process is endothermic, its rate can be small.

The data input necessary to study the astrophysical nucleosynthesis processes comes from experimental measurements and theoretical predictions. Our code uses the nuceq library to compute the nuclear statistical equilibria established for the thermonuclear fusion reactions. The abundances are calculated under the constraints of nucleon number conservation and charge neutrality, and the appropriate correction function to account for degeneracy of relativistic species is used. The reaction data were downloaded from JINA reaclib online database (http://www.jinaweb.org), prepared for studies of the nuclear masses and nuclear partition functions, and for computations of the nuclear statistical equilibria.

4. Results

The mass fraction of heavy nuclei was computed at every radius of the accretion disk, given the profiles of its density, temperature and electron fraction. In Figure 2, we show the resulting distributions of the most abundant isotopes of heavy elements synthesized in this plasma. An exemplary model is presented and its parameters are: accretion rate of \( \dot{M} = 0.1 M_\odot / s \) and black hole spin \( a = 0.9 \).
Figure 2: The mass fractions of heavy elements synthesized in the accretion disk in GRB engine. The model parameters are: accretion rate of $\dot{M} = 0.1 M_\odot / s$ and black hole spin $a = 0.9$. Left panel shows the abundance distribution of free protons and neutrons (dashed lines), as well as Helium, and the most abundant isotopes of Nickel, Iron, and Cobalt. Right panel shows the distribution of the most abundant isotopes of Silicon, Sulphur, Chlorium, Argonium, Manganium, Titatnium, Vanadium, and Cuprum.

For the accretion rate of $0.1 M_\odot s^{-1}$, the abundance of $^4$He is large with a value up to $\sim 260 r_g$ and then decreases throughout the disk; there is some fraction of $^3$He, Deuterium, and Tritium. The next abundant isotopes are $^{28}$Si - $^{30}$Si, $^{31}$P, $^{32}$S - $^{34}$S, then $^{35}$Cl, and $^{36}$Ar - $^{38}$Ar. Further, synthesized isotopes are $^{39}$K, $^{40}$Ca - $^{42}$Ca, $^{44}$Ti - $^{50}$Ti, $^{47}$V - $^{52}$V, $^{48}$Cr - $^{54}$Cr, and $^{51}$Mn - $^{56}$Mn. The most abundant Iron isotopes formed in the disk are $^{52}$Fe through $^{58}$Fe; Cobalt is formed with isotopes $^{54}$Co through $^{60}$Co, and Nickel isotopes are $^{56}$Ni through $^{62}$Ni. The heaviest most abundant isotopes in our disk are $^{59}$Cu through $^{65}$Cu. Further, there is a smaller fraction of Zinc, $^{60}$Zn - $^{64}$Zn, with a mass fraction above $10^{-5}$. These heavy elements are generally produced outside 300-400 $r_g$. Inside this radius, the disk consists of mainly free neutrons and protons with some fraction of Helium. The mass fraction of free neutrons is smaller than that of protons, and free neutrons disappear above $\sim 300 r_g$.

In comparison to the model with small accretion rate presented above, the conditions in the disk with accretion rate of $1.0 M_\odot s^{-1}$, are such that the mass fraction of free neutrons is larger than that of free protons inside $\sim 200 r_g$ and comparable to a proton mass fraction up to $\sim 500 r_g$. In both models, the heavy elements dominate above $\sim 550 r_g$ (see Janiuk 2014).

5. Discussion

The different properties of central engines in the two classes of bursts, namely short and long GRBs, which we accounted for here using two distinct values of accretion rate in their central
engines, determine qualitatively the details of the nucleosynthesis process. This should be taken into account in the statistical studies of the observed phenomena (Gehlers et al. 2008).

For the accretion rate of $0.1 M_\odot / s$, our calculations show the significant proton excess in the disk above $\sim 250 r_g$. The wind ejected at this region may therefore provide a substantial abundance of light elements, Li, Be, and B. The high-accretion rate disk, on the other hand, produces neutron rich outflows and forms heavy nuclei via the $r$-process. As we show here, the outflows ejected from the innermost $100 r_g$ in the high-accretion rate disks are also significantly neutron rich. Therefore these neutron-loaded ejecta, which are accelerated via the black hole rotation, feed the collimated jets at a large distance from the central engine. This has important implications for the observed GRB afterglows, which are induced by the radiation drag (Metzger et al. 2008), and collisions between the proton-rich and neutron-rich shells within the GRB fireball (Beloborodov 2003).

The signatures of heavy elements synthesis have been found in a number of supernovae associated with gamma ray bursts and their underlying spectra (e.g., Iwamoto et al. 1998, Kawai et al. 2006) or lightcurves (e.g., Nakamura et al. 2001). The isotopes synthesized in the GRB central engine accreting torus and its outflows during the prompt emission phase, should be detectable via the X-ray emission that originates from their radioactive decay. These isotopes, such as Titanium $^{54} Ti$, $^{57} Co$, $^{62} Cu$, $^{65} Ga$, $^{60} Zn$, $^{49} Cr$, $^{65} Co$, $^{61} Co$, $^{61} Cu$, and $^{44} Ti$, might give the signal in the 12-80 keV energy band, which could be observed by current instruments of good energetic resolution, e.g. by NuSTAR (e.g, Kouveliotou et al. 2013).

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