Abstract: In this paper, an intelligent sliding mode controlled voltage source inverter (VSI) is developed to achieve not only quick transient behavior, but satisfactory steady-state response. The presented approach combines the respective merits of a nonsingular fast terminal attractor (NFTA) as well as an adaptive neuro-fuzzy inference system (ANFIS). The NFTA allows no singularity and error states to be converged to the equilibrium within a finite time, while conventional sliding mode control (SMC) leads to long-term (infinite) convergent behavior. However, there is the likelihood of chattering or steady-state error occurring in NFTA due to the overestimation or underestimation of system uncertainty bound. The ANFIS with accurate estimation and the ease of implementation is employed in NFTA for suppressing the chatter or steady-state error so as to improve the system's robustness against uncertain disturbances. Simulation results display that this described approach yields low distorted output wave shapes and quick transience in the presence of capacitor input rectifier loading as well as abrupt connection of linear loads. Experimental results conducted on a 1 kW VSI prototype with control algorithm implementation in Texas Instruments DSP (digital signal processor) support the theoretic analysis and reaffirm the robust performance of the developed VSI. Because the proposed VSI yields remarkable benefits over conventional terminal attractor VSIs on the basis of computational quickness and unsophisticated realization, the presented approach is a noteworthy referral to the designers of correlated VSI applications in future, such as DC (direct current) microgrids and AC (alternating current) microgrids, or even hybrid AC/DC microgrids.

Keywords: intelligent sliding mode; voltage source inverter (VSI); DC microgrid; adaptive neuro-fuzzy inference system (ANFIS); chattering

1. Introduction

Distributed energy resources (DERs)-based microgrids can yield electricity to the grid and once the power grid goes out unexpectedly. Such microgrids assure the reliability of electricity supply with the presence of sensitive loads [1–3]. The DERs require power electronic interfaces for the connection of the microgrid. Generally, we can group the microgrids into two types, i.e., DC microgrids and AC microgrids. Owing to better compatibility, higher efficiency and robust stability, the DC microgrids have gained more and more research interest. In a DC microgrid, voltage source inverters can be adopted as an interface between the DC grid and typical AC loading. The inverter works in two different modes. One is island mode, where the inverter can be regarded as a voltage source. It can afford the devices with sine voltage, and pulse width modulated control can be used in this mode. The other operation mode allows the delivery of the current to the grid, and another control scheme can be adopted like hysteresis current control. Using reference voltage tracking techniques, the voltage source inverter (VSI) can control the voltage quality of the distribution networks [4,5]. Diverse methodologies can be found in publications, namely the H-infinity approach, the deadbeat technique and the fractional order repetitive controller [6–8]. However, there is a compromise between the...
transient response and the steady-state response. Sliding mode control (SMC) offers insensitivity against parametric uncertainties and external disturbances [9–11]. The SMC has been attempted to design VSI [12–21]. The grid-tied inverter controlled by the fixed switching frequency SMC is developed. A good steady-state response can be obtained, but chatter and poor transience exist [12,13].

The ingenious combination of a proportional-resonant and a SMC is suggested to improve the system response of the single-phase inverter. Even if the transient behavior of system performance is effectively improved, the presented algorithm leads to steady-state errors [14,15]. A control method based on the multi-slope sliding surface is also employed for single-phase inverter design. The transient and steady state behavior is compromising while feeding nonlinear loads [16,17]. Using a stable switching manifold to enhance the robustness of a grid-connected inverter has been reported. The state trajectory cannot touch the predetermined sliding manifold in a fast finite time, thus displaying output-voltage distortion [18,19]. Additionally, an improved sliding mode controller for a photovoltaic inverter is presented by [20,21]. Although such an improved methodology has shown fast transience and satisfactory steady-state response, the problem of the chattering still appears around the sliding manifold. It is important to heed that the long convergence time and the chattering phenomenon exist in the above-mentioned conventional SMCs.

During the past few years, terminal attractors (TAs) have attracted growing interest for application in different areas [22,23]. TAs can provide finite time tracking while still preserving the robustness of the conventional SMC [24,25]. Unfortunately, TAs still produce the difficulties in singularity and chattering. The singularity may cause the system states to converge to zero in infinite time. For the sake of suppressing the singularity, the nonsingular fast terminal attractor (NFTA) is introduced in this paper. The NFTA makes tracking error on the sliding surface converge to zero within a finite time, thus obtaining closed-loop stability. For practical applications, unmodeled dynamic uncertainty and parametric plant perturbation, and external disturbances are not so easy to estimate beforehand. If the uncertain boundary conditions are somewhat big or small, a large amount of chattering or steady-state error happens, losing the existence and invariance of the sliding mode. Former works have recommended high-gain feedback to reject perturbations resulting from boundary uncertainties. Employing large constant gain is easy to implement, but there is unpopular chattering or steady-state error occurring in the plant system [26,27]. Many studies have found that the chattering or steady-state error can be attenuated by the use of the observer method or hybrid control strategy [28–35]. A low-cost microcontroller under hybrid control has been presented. The proposed controller effectively reduces the chattering, but there is a steady-state error in response to sudden load disturbance [28,29]. The improved observer due to higher accuracy and stronger robustness is also introduced into sliding mode design for a servo system. Though good steady-state behavior can be seen, the output waveform shows a slow dynamic response during the transient stage [30,31]. To withstand parameter variations and load interferences, a sliding control with an adaptive law combined with an expert semantic description is used to control a grid-connected inverter. The resulting waveforms display a fast transient characteristic, however a large amount of chattering still exists in this presented method [32,33]. By the application of a typical microgrid, the developed system with the association of fuzzy and SMC can obtain improved performance in steady-state and transient responses. Unfortunately, such a methodology is complex and needs heavy calculation [34,35]. To address the problem of the chattering or steady-state error, an adaptive neuro-fuzzy inference system (ANFIS) incorporating both neural networks and fuzzy logic principles is employed in this paper. [36,37]. A neural network is a kind of supervised learning algorithm, which uses a historical dataset to forecast future values. In fuzzy logic, the control signal is produced from the firing of the rule base. Using this hybrid-learning algorithm, the difference between demanded and real outputs is minimized, therefore weakening the chattering when the estimation value exceeds the uncertain system boundary, or reducing steady-state error when the estimation value falls short of the uncertain system boundary [38–40]. With the association of ANFIS and NFTA, the proposed approach can yield a VSI feedback control with many advantages, such as finite-time fast convergence without
inflicting any singularity, fast dynamic response, low THD (total harmonic distortion), chattering reduction and less steady-state error in the presence of transient loading and steady-state loading. Comparison and discussion of the results in simulation and experiment are provided to corroborate the applicability and feasibility of the proposed approach.

2. Mathematical Representation of VSI

Figure 1a shows a single-phase VSI that is made up of power MOSFET (metal-oxide-semiconductor field-effect transistor), an LC (inductor capacitor) filter and load. The symbol $V_s$ represents the DC bus voltage, $v_o$ denotes the output voltage, $i_o$ is the output current, and $L$, $C$, and $R$ are the inductor, capacitor and load, respectively. As shown in Figure 1b, $v_{inv}$ stands for a pulse width modulated voltage of magnitude $V_s$ (or $-V_s$) with $\Delta T$ centered in the sampling interval $T$. Since the inverter output voltage is a sinusoidal waveform, the $v_o$ has to follow a desired sinusoidal waveform. For example, for a rms (root mean square) 110 V with a specified frequency of 60 Hz utility power, the $v_o$ expected voltage waveform will be $\sqrt{2} \cdot 110 \cdot \sin(2\pi f \cdot t)$. In other words the output voltage $v_o$ of the VSI can be generally expressed as $\sqrt{2} \cdot V_{rms} \cdot \sin(2\pi f \cdot t)$ in which $V_{rms}$ and $f$ are the root-mean-square and the frequency values of output voltage, respectively. According to the control theory literature [41], we find that the design of the VSI is intrinsically a typical tracking control problem. By choosing $x_1 = v_o$ and $x_2 = \dot{v_o}$, the dynamic equation of the VSI is derived as:

$$
\begin{bmatrix}
\dot{x}_1 \\
\dot{x}_2
\end{bmatrix} =
\begin{bmatrix}
0 & 1 \\
-\frac{1}{LC} & -\frac{1}{RC}
\end{bmatrix}
\begin{bmatrix}
x_1 \\
x_2
\end{bmatrix} +
\begin{bmatrix}
0 \\
\frac{1}{RC}
\end{bmatrix} v_{inv}
$$

(1)

where $a_1 = -1/\mathit{LC}$, $a_2 = -1/\mathit{RC}$, $b = 1/\mathit{LC}$ and $v_{inv} = (\Delta T/T) \cdot V_s$. The control signal $u$ is equal to $d \cdot V_s$ (time-averaging technique, see [42,43]), where $d$ is the duty ratio of switching ranging from $-1$ to $1$ and $V_s$ denotes the DC bus voltage.

![Figure 1](image)

**Figure 1.** Construction of voltage source inverter (VSI) (a) Circuit diagram ($V_s$: DC-bus voltage, $v_{inv}$: equivalent output voltage of pulse width modulation, $v_o$: output voltage, $i_o$: output current and $R$: load); (b) PWM (pulse width modulation) pattern ($T$: sampling interval and $\Delta T$: width).
Letting the desired output voltage $v_d$ be $\sqrt{2} \cdot V_{rms} \cdot \sin(2\pi f \cdot t)$, new state variables are defined as:

$$
\begin{align*}
  e_1 &= x_1 - v_d \\
  e_2 &= x_2 - \tilde{v}_d
\end{align*}
$$

By the use of (1) and (2), the error dynamics of a VSI is written as:

$$
\begin{bmatrix}
  \dot{e}_1 \\
  \dot{e}_2
\end{bmatrix} = 
\begin{bmatrix}
  0 & 1 \\
  -a_1 & -a_2
\end{bmatrix} 
\begin{bmatrix}
  e_1 \\
  e_2
\end{bmatrix} + 
\begin{bmatrix}
  0 \\
  b
\end{bmatrix} u + 
\begin{bmatrix}
  0 \\
  \Theta
\end{bmatrix}
$$

where $\Theta = -a_1 v_d - a_2 \tilde{v}_d - \tilde{v}_d$ is the uncertainties, such as plant parameter variations, external disturbances and measurement noises. Apparently, we can design $u$ to allow $e_1$ and $e_2$ to converge to zero, i.e., $x_1 = v_d$ and $x_2 = \tilde{v}_d$. In the path-tracking control design, it is worth pointing out that once $e_1$ and $e_2$ have fast finite time convergence, the system will achieve good performance, strong robustness and infinite stability. Based on the motive for fast finite time convergence and fast convergence property inherited from NFTA, the NFTA VSI will be able to offer not only good dynamic response (fast convergence), but also higher accuracy control (lower THD and tracking error). However, the load of the VSI is not fixed, and the system still has chattering or steady-state error problems when exposed to large step change in loading conditions, extreme parameter variations or highly non-linear loads; the ANFIS can be suggested as an effective way to resolve the chattering or steady-state error in practical applications [44-50]. Therefore, an intelligent robust tracking controller with the masterly combination of the NFTA and ANFIS compensation for high performance VSI will be presented and the design of the controller is as follows.

3. Proposed Control Approach of VSI

Problem Statement

Firstly, in this section, the problem statement of the nonlinear system using classic finite-time convergent SMC is presented, and then the proposed controller is designed.

The following second-order nonlinear dynamics are defined as:

$$
\begin{align*}
  \dot{x}_1 &= x_2 \\
  \dot{x}_2 &= f(x) + g(x)u + \Theta(x)
\end{align*}
$$

where $x = \begin{bmatrix} x_1 & x_2 \end{bmatrix}^T$ is the state vector, $f(x)$ and $g(x)$ stand for known nonlinear functions, $u$ represents the control input, and $\Theta(x)$ symbolizes unknown external disturbances, which are assumed to be bounded as $\|\Theta(x)\| < \xi$; here, $\xi$ is positive constant.

A conventional TA can be written as:

$$
\sigma = x_2 + \beta|x_1|^{\gamma} \text{sgn}(x_1)
$$

where $\beta$ is a positive real number and $0 < \gamma < 1$. Although TAs can achieve finite-time stability of the system, both the performance and convergence speed of the system are deteriorated while an initial system state stands off the equilibrium. FTA attempts to overcome this problem as follows:

$$
\sigma = x_2 + \alpha x_1 + \beta|x_1|^{\gamma} \text{sgn}(x_1)
$$

where $\alpha$ is a positive real number. When $x_1$ is far from the zero, the characteristic of the system becomes $\sigma \approx x_1 + \alpha x_1$, thus yielding exponential stability. When $x_1$ is close to zero, the FTA is introduced and allows the fast convergence rate of system behavior, which gives rise to finite-time convergence. However, there is still the problem of the singularity appearing in FTA for practical applications.
Eventually for the error dynamics (3), the NFTA can be constructed to ensure faster convergence and precise control without the singularity problem as follows [11,24,25]:

$$\sigma = e_1 + \alpha |e_1|^{\rho_1} \text{sgn}(e_1) + \beta |e_2|^{\rho_2} \text{sgn}(e_2)$$  \hspace{1cm} (7)

where $\alpha > 0$, $\beta > 0$, $\rho_1 > 1$ and $1 < \rho_2 > 2$.

The feedback control law of NFTA is designed as:

$$u(t) = u_e(t) + u_s(t)$$  \hspace{1cm} (8)

with:

$$u_e(t) = -b^{-1}[a_1e_1 + a_2e_2 + \frac{1}{\beta \rho_2}|e_2|^{2-\rho_2} \text{sgn}(e_2) + \frac{\alpha \rho_1 |e_1|^{\rho_1-1}}{\beta \rho_2}|e_2|^{2-\rho_2} \text{sgn}(e_2)]$$  \hspace{1cm} (9)

$$u_s(t) = -b^{-1}[(\xi + \tau) \text{sgn}(\sigma)]$$  \hspace{1cm} (10)

where $\tau > 0$, $u_e$ is equivalent control for a nominal system without singular phenomenon, and $u_s$ stands for sliding control that arrests external load disturbance. Thereby, the states reach $\sigma = 0$ and finite-time convergence is provided.

**Proof.** Choose the following Lyapunov candidate function

$$V = 0.5\sigma^2$$  \hspace{1cm} (11)

Calculating the derivative of $V$ along the trajectories of (3) gives:

$$\dot{V} = \sigma \dot{\sigma} = \sigma (\dot{e}_1 + \alpha |e_1|^{\rho_1-1} \dot{e}_1 + \beta |e_2|^{\rho_2-1} \dot{e}_2)$$  \hspace{1cm} (12)

Owing to the existence of $\sigma \neq 0$, $e_2 \neq 0$ and $||\Theta|| < \xi$, $\dot{V} \leq -\tau |\sigma| < 0$, which infers that the $\sigma$ in (12) can be converged to the equilibrium point within a finite time, a finite system-state convergence time of (3) yields while $\sigma$ is reached. However, the NFTA may undergo chattering or steady-state error when the load is a severely uncertain circumstance. In order to get rid of the chattering effect, the ANFIS displayed as (13)–(21) is integrated into the control law (8) in the VSI design. Figure 2 plots a common architecture of an ANFIS, which uses the Takagi–Sugeno type fuzzy model with two if-then rules as the following statements [36]:

**Rule 1:** If $e_1$ is $A_1$ and $e_2$ is $B_1$ then $h_1 = p_1e_1 + q_1e_2 + r_1$  \hspace{1cm} (13)

**Rule 2:** If $e_1$ is $A_2$ and $e_2$ is $B_2$ then $h_2 = p_2e_1 + q_2e_2 + r_2$  \hspace{1cm} (14)

where $A_i$ and $B_i$ symbol the fuzzy sets in the antecedent, and $p_i$, $q_i$ and $r_i$ signify the design parameters decided in the training duration.

**Layer 1:** A node function is employed through every node $i$ as:

$$O^1_i = \mu_{A_i}(e_1), \; i = 1, 2$$  \hspace{1cm} (15)

$$O^1_i = \mu_{B_i}(e_2), \; i = 3, 4$$  \hspace{1cm} (16)

where $\mu_{A_i}$ and $\mu_{B_i}$ can use fuzzy membership functions.

**Layer 2:** Every node calculating the rule’s firing strength by the multiplier is as follows:
where \( w_i \) stands for the output with the firing strength of each rule.

Layer 3: Node \( i \) computes the proportion between \( i \)th rule’s firing strength and the sum of all rules’ firing strengths. The normalized firing strengths yield:

\[
O^3_i = \bar{w}_i = w_i/(w_1 + w_2), \quad i = 1, 2
\]  

Layer 4: Every node \( i \) yields the following function:

\[
O^4_i = \bar{w}_i h_i = \bar{w}_i (p_i e_1 + q_i e_2 + r_i), \quad i = 1, 2
\]  

where \( \bar{w}_i \) stands for the output of the previous layer, and \( p_i, q_i \) and \( r_i \) parameters are fuzzy consequent parameters.

Layer 5: The single node of this layer deals with the overall output, summing up to all entered signals as follows:

\[
O^5_i = \sum_{i=1}^{2} \bar{w}_i h_i = (w_1 h_1 + w_2 h_2)/(w_1 + w_2)
\]  

The output \( h \) shown in Figure 2 can be formulated as:

\[
h = (\bar{w}_1 e_1)p_1 + (\bar{w}_1 e_2)q_1 + (\bar{w}_1 r_1) + (\bar{w}_2 e_1)p_2 + (\bar{w}_2 e_2)q_2 + (\bar{w}_2 r_2)
\]  

\[h = (\bar{w}_1 e_1)p_1 + (\bar{w}_1 e_2)q_1 + (\bar{w}_1 r_1) + (\bar{w}_2 e_1)p_2 + (\bar{w}_2 e_2)q_2 + (\bar{w}_2 r_2)\]

**Figure 2.** Architecture of the adaptive neuro-fuzzy inference system (ANFIS) (\( e_i \): input, \( A_i, B_i \): linguistic labels, \( w_i \): weight and \( h_i \): output, for \( i = 1, 2 \)).

In summary, the ANFIS architecture is formed by the fuzzy logic model and the artificial neural network, so that the mapping of the inputs to the output is performed. In Figure 2, the basic construction of the ANFIS is illustrated for the first-order Takagi-Sugeno interface system. It is made up of two inputs \( e_1 \) and \( e_2 \), and one output \( h \). The first and second layers are regarded as the fuzzification and rule layers, respectively. The first layer deals with the mapping process of the input variable corresponding to each membership functions, and the second layer calculates the rules antecedents. The third layer is called the normalization layer, and the fourth and fifth layers respectively provide the tasks of defuzzification and output. The third layer can normalize the strengths of the rules and then the fourth hidden layer determines the consequents of the rules. Finally, the output layer counts the complete output as the sum of entire arrived signals. In short, the ANFIS permits the choice of the rule base which adapts to the system circumstance. The rule base can be
chosen using a backpropagation neural network algorithm. For the sake of increasing the performance, the feature of the fuzzy logic provides the approximation of a nonlinear system via IF-THEN rules that is inherited in this modeling technology. Such a combined method makes ANFIS a universal estimator.

4. Simulation and Experimental Results

The simulation and experimental verification of the presented approach are carried out on a VSI with specifications shown in Table 1. For the sake of the analysis and comparison to the dynamic and steady-state response, the overall system is tested under varying operating conditions, namely step-load changing, filter parameter variations and rectifier loads.

| Table 1. VSI system parameters. |
|---------------------------------|
| **Filter Inductor** | $L = 0.1 \text{ mH}$ |
| **Filter Capacitor** | $C = 2 \mu\text{F}$ |
| **Resistive Load** | $R = 12 \Omega$ |
| **DC link Voltage** | $V_s = 200 \text{ V}$ |
| **Output Voltage and Frequency** | $v_o = 110 \text{ V}_{\text{RMS}}, f = 60 \text{ Hz}$ |
| **Switching Frequency** | $f_s = 12 \text{ kHz}$ |

In the simulated waveforms of Figure 3, obtained using the proposed approach, the disturbances caused by the connection of a rated resistive load are presented. After a slight transience, the output voltage quickly recovers to the demanded rms value of 110 V. A good dynamic response and the ability of abrupt disturbance rejection are yielded. Inversely, Figure 4 represents simulated output voltage and output current subject to the same load circumstance obtained using conventional SMC. The large voltage drop and slow recovery time occur while the output voltage has a noticeable oscillation at the back of the transient termination. Figure 5 indicates that the proposed VSI encounters filter parameter variations from 20% to 200% of nominal values with a 12 ohm resistor. The proposed approach is capable of tolerating severe plant parameter variations. Therefore, the simulated output voltage produces a low distorted sinusoidal waveform (%THD is 0.02%). However as expected, the conventional SMC VSI (shown in Figure 6) exhibits low steady-state accuracy with periodic distortion in the simulated output voltage. Namely, it has a high sensitivity to filter parameter variations, resulting in a great deal of voltage harmonics (%THD is 14.32%). Table 2 gives the drop and %THD of the proposed VSI and the conventional SMC VSI in the presence of step load changes and filter parameter variations. A step change in a resistive load (from no load to full load) has been carried out for the experimental waveforms (as shown in Figure 7) obtained using the proposed approach. Under the same load testing condition, Figure 8 depicts the experimental output voltage and output current obtained using the conventional SMC. Comparing of the results from the two figures, the proposed approach yields good compensation for voltage drop mitigation, namely less voltage drop and faster transient recovery time. The output voltage waveform corroborates the robustness of the proposed approach in the presence of load transients. There is no apparent sinusoidal jitter after the occurrence of the transience. Surely, the conventional sliding mode controlled VSI unmask the performance deterioration—for instance, a large voltage drop when firing at an angle of 90°, slow dynamic response and noticeable vibration behind the transient resumption. To authenticate the performance of the proposed approach under the nonlinear load, Figure 9 plots experimental waveforms in response to a full-wave rectified resistive load (40 Ω) with a DC-side capacitor filter (330 μF). The output voltage of the VSI is close to sine wave and has a low percent THD of 1.82%, which is superior to the five percent industrial standard. Same as the nonlinear load case, the experimental waveforms obtained using the conventional SMC are depicted in Figure 10. The experimental construction is given in Figure 11. The output voltage with a high %THD of 10.21% distorts the resulting waveform, thus leading to large deviation and an unsatisfactory steady-state response. The output voltage drop and %THD of the proposed controlled VSI, as well as the conventional VSI, are listed in Table 3 under step load changes.
and nonlinear loads. Finally, the improvement of the proposed method really exceeds conventional SMC and is also better than FTA [25].

**Figure 3.** Simulated output waveforms at step-load changing conditions obtained using the proposed approach (Vo: output voltage; io: output current).

**Figure 4.** Simulated output waveforms at step-load changing conditions obtained using the conventional sliding mode control (SMC).
Figure 5. Simulation output waveforms against filter parameter variations obtained using the proposed approach.

Figure 6. Simulation output waveforms against filter parameter variations obtained using the conventional SMC.

Table 2. Simulation comparison of output voltage drop and %THD.

| Proposed Approach | Step-load changing | Filter parameter variations | Voltage drop | %THD |
|-------------------|--------------------|-----------------------------|--------------|------|
|                   |                    |                             | 4.6 $V_{\text{rms}}$ | 0.02% |
| Conventional SMC  |                    |                             | 22.9 $V_{\text{rms}}$ | 14.32% |
**Figure 7.** Experimental output waveforms at step-load changing conditions obtained using the proposed approach (vertical: 100 V/division and 20 A/division, horizontal: 5 ms/division).

**Figure 8.** Experimental output waveforms at step-load changing conditions obtained using the conventional SMC (vertical: 100 V/division and 20 A/division, horizontal: 5 ms/division).

**Figure 9.** Experimental output waveforms under rectifier load obtained using the proposed approach (vertical: 100 V/division and 20 A/division, horizontal: 5 ms/division).

**Figure 10.** Experimental output waveforms under rectifier load obtained using the conventional SMC (vertical: 100 V/division and 20 A/division, horizontal: 5 ms/division).
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**5. Conclusions**

This paper has presented a hybrid controller, which is the association of a robust control technology and machine learning algorithm, to control a voltage source inverter. In this proposed control method, a finite convergence time NFTA offers strong robustness and fast finite-time stability without any singularity. However, if the system is exposed to parametric nonlinearities, parameter variations or unmodelled dynamics, it is not easy to obtain these accurate values completely in practice. As a result, chattering or steady-state error occurs due to the overestimated or underestimated uncertainty bound. The ANFIS with accurate bound estimation is used to tackle and accommodate the uncertain perturbations. The Lyapunov stability criterion displays that the combination of NFTA and ANFIS guarantees the practical finite-time stability of the tracking errors with greater robustness to system uncertainties. Simulations and experiments illustrate that the proposed approach yields very good steady-state and dynamic characteristics under various operating circumstances, such as load step changes, filter parameter variations, and rectifier-type loads.

**Author Contributions:** E.-C. C. conceived the algorithm, designed the circuit, and performed control system simulations. In addition, E.-C. C. carried out experiments, analyzed the results, wrote the paper and revised it for submission.

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