Direct proton decay of the isoscalar giant dipole resonance in $^{208}$Pb

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Abstract

The excitation and subsequent proton decay of the isoscalar giant dipole resonance (ISGDR) in $^{208}\text{Pb}$ have been investigated via the $^{208}\text{Pb}(\alpha, \alpha'p)^{207}\text{Tl}$ reaction at 400 MeV. Excitation of the ISGDR has been identified by the difference-of-spectra method. The enhancement of the ISGDR strength at high excitation energies observed in the multipole-decomposition-analysis of the singles $^{208}\text{Pb}(\alpha, \alpha')$ spectra is not present in the excitation energy spectrum obtained in coincidence measurement. The partial branching ratios for direct proton decay of ISGDR to low-lying states of $^{207}\text{Tl}$ have been determined and the results are compared with predictions of continuum random-phase-approximation (CRPA) calculations.

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The compression-mode isoscalar giant dipole resonance (ISGDR), like the isoscalar giant monopole resonance (ISGMR), provides a direct method to obtain the incompressibility of the nucleus and of nuclear matter \((K_{\text{nm}})\). The first direct evidence for the ISGDR in nuclei was obtained in \(^{208}\text{Pb}\) with the “difference-of-spectra” technique (DOS) in inelastic scattering of 200 MeV \(\alpha\)-particles. Subsequently, the Texas A & M group obtained the ISGDR strength distributions in several nuclei using a multipole-decomposition analysis (MDA) of the background-subtracted inelastic \(\alpha\)-scattering spectra at 240 MeV. However, a major concern was that the centroids of the ISGDR strength distribution from these studies were found to be consistently lower than those predicted by calculations employing the same value of nuclear incompressibility that correctly reproduced the centroid energies of the ISGMR strength distributions. This ambiguity has been resolved by more precise and instrumental-background-free measurements of ISGDR strength distributions using inelastic scattering of 400 MeV \(\alpha\) particles. The value of the nuclear incompressibility, \(K_{\text{nm}}\), obtained from the ISGDR data is now fully consistent with that from the ISGMR data. However, a problem has remained with the ISGDR strength extracted from the aforementioned singles measurements: significantly large E1 strength was observed at the higher-excitation energy part of the main ISGDR peak in all nuclei under investigation (see, for example, Fig. 3 of Ref. and Fig. 4 of Ref. ). This extra strength was attributed to contributions to the continuum from three-body channels, such as pick-up/breakup reactions. These processes form part of the continuum and lead to spurious ISGDR contributions in the MDA because of the forward-peaked nature of their angular distributions. The effect is significant in the high excitation-energy region where the associated cross sections are very small. Incidentally, a similar increase at higher excitation energies has been reported in the E0 strength in \(^{12}\text{C}\) as well when a MDA was carried out without subtracting the continuum from the excitation-energy spectra.

A primary motivation of the present study has been to address the aforementioned problem of excess ISGDR strength at high excitation energies apparent in the singles measurements. Investigations of the direct proton-decay channels of ISGDR in the \((\alpha, \alpha'p)\) reaction renders this eminently possible. In general, decay studies afford several advantages over the singles measurements. Firstly, events in the continuum that are associated with forward-peaking processes, such as quasifree scattering and pick-up/breakup reactions, are effectively suppressed by putting a coincidence condition with decay protons at backward angles; the
contributions from the resonance, however, remain in the true coincidence spectra (subject, of course, to the decay probabilities). Secondly, by gating on the particle decay channels populating specific single-hole states in the daughter nuclei, the resonance states, which are comprised of states with 1p-1h configurations, are enhanced, providing a detailed look at the decay properties, such as the relative population and strength of particle-decay channels from the resonance to the final hole states in the daughter nucleus. This can provide crucial information to test the available microscopic model calculations.

In the past, direct proton-decay from the ISGDR in $^{208}$Pb has been measured using $(\alpha,\alpha'p)$ reaction at a bombarding energy of 200 MeV [13, 14]. In these measurements, a new $L = 2$ resonance was reported at $E_x = 26.9 \pm 0.7$ MeV with a width of $6.0 \pm 1.3$ MeV; this has been suggested as the $L = 2$ compression-mode resonance [15]. In a subsequent neutron-decay measurement at the same energy, although the population of the low-lying states through direct neutron decay of the ISGDR region was found to be significant and well separated from the statistical decay, the direct neutron decay from the continuum region above the ISGDR energy did not show any significant population to the final single-hole states [16]. The present investigation not only provides further information on the decay of the ISGDR to specific particle-hole states, but also allows another look at the aforementioned $L = 2$ resonance which had not been identified in any of the singles measurements.

Angular distributions of differential cross sections of $(\alpha,\alpha')$ reactions strongly depend on the transferred angular momentum $L$. This is evident in Fig. 1, where the differential cross sections for various multipoles ($L \leq 3$) for the $^{208}$Pb$(\alpha,\alpha')$ reaction at $E_\alpha = 400$ MeV calculated in DWBA in the angular range $0^\circ$–$3^\circ$ for excitation energy $E_x = 22.5$ MeV are seen to be clearly distinct from each other. The cross section for ISGDR ($L = 1$) is maximal at $1.28^\circ$; the cross sections for the $L = 2$ and $L = 3$ modes, on the other hand, are more or less constant over $0^\circ$–$3^\circ$. By subtracting the differential cross section near $0^\circ$ from that at small finite angles ($1^\circ$–$1.5^\circ$), one can identify the ISGDR strength since the contributions from $L = 2$ and $L = 3$ modes would be essentially eliminated in the subtraction process. This forms the basis of the DOS technique which has been successfully employed in the past to identify GMR and ISGDR strengths in small-angle inelastic scattering spectra [2].

Guided by these calculations for the cross sections, measurements were performed at the ring cyclotron facility of Research Center for Nuclear Physics (RCNP), at Osaka University, which provided an $\alpha$-particle beam with an energy of 400 MeV. The $\alpha$-beam bombarded a
FIG. 1: Differential cross sections for exciting isoscalar giant resonances via the $^{208}\text{Pb}(\alpha, \alpha')$ reaction calculated in DWBA, assuming 100% exhaustion of the energy-weighted sum rules for the respective transitions. The calculations were performed at $E_\alpha = 400$ MeV for excitation energy $E_x = 22.5$ MeV. The curves drawn are for ISGMR (solid), ISGDR (dotted), ISGQR (dashed), and HEOR (dash-double-dotted).

$^{208}\text{Pb}$ target with a thickness of $10.1 \text{ mg/cm}^2$. The ejectiles were momentum analyzed by the magnetic spectrometer Grand Raiden [17] which was set at $0^\circ$ to the beam direction covering a scattering angular range $0^\circ$ to $1.8^\circ$; the total solid angle in this setting was $1.2 \text{ msr}$. The “energy bite” of the spectrometer at this energy is $30 \text{ MeV}$; data were, therefore, obtained over the excitation-energy range $\sim 4 \sim 34 \text{ MeV}$. Decay protons were detected in coincidence with inelastically scattered $\alpha$ particles with sixteen silicon solid-state detectors, each with a thickness of $5.0 \text{ mm}$, placed at angles of $112.5^\circ$, $135^\circ$ and $157.5^\circ$ with respect to the beam direction. The energy calibrations of the singles ($\alpha, \alpha'$) spectra and of decay-proton energies measured with solid-state detectors were carried out by using the $^{12}\text{C}(\alpha, \alpha')$ and $^{12}\text{C}(\alpha, \alpha'p)$ reactions.

Fig. 2(a) shows the two-dimensional scatter plot of decay-proton energy versus the target excitation energy. One can clearly see several loci corresponding to the proton-decay channels populating the low-lying final states in $^{207}\text{Tl}$. Fig. 2(b) is essentially the same as Fig. 2(a) but shows the correlation between the energies of the final states in $^{207}\text{Tl}$ and the target excitation energy in $^{208}\text{Pb}$ instead; Fig. 2(c) shows the excitation-energy spectrum of $^{208}\text{Pb}$ in coincidence with proton decay to low-lying states in $^{207}\text{Tl}$. Fig. 2(d) shows the final-state spectrum of $^{207}\text{Tl}$ for proton decay.
FIG. 2: (a) Two-dimensional scatter plot of the decay proton energy $E_p$ versus excitation energy $E^*$ in $^{208}$Pb. (b) Same as (a), but the proton energies have been converted to excitation energies in $^{207}$Tl. The loci correspond to decay-events to specific final states in $^{207}$Tl. (c) The projection of data in Fig. 2 (b) onto the excitation-energy axis in $^{208}$Pb for the indicated excitation-energy range in $^{207}$Tl. The spectrum shows primarily the ISGDR strength distribution. (d) The projection of data in Fig. 2 (b) onto the final-state excitation-energy axis in $^{207}$Tl. The first peak is a composite of the ground state and the 0.35 MeV excited state; the second peak is a combination of the 1.35 MeV and 1.67 MeV excited states.
FIG. 3: The final-state spectrum of the low-lying proton-hole states in $^{207}$Tl generated by gating on the $(\alpha, \alpha')$ events in the ISGDR excitation-energy region at the scattering angles $\theta_{c.m.} = 1.0^\circ - 1.5^\circ$.

In Fig. 3, the final-state spectrum has been decomposed to show the relative population of various low-lying states. The FWHM of individual states in the final-state excitation-energy spectra for $^{207}$Tl was $\sim 650$ keV, as obtained from multiple-peak fitting of the excitation-energy spectrum; it was not possible, hence, to clearly resolve clearly the individual final states in $^{207}$Tl. However, there are two enhanced bumps, denoted as groups A and B, attributed to proton decays to the $(3s_{1/2} + 2d_{3/2})$ hole states and to the $(1h_{11/2} + 2d_{5/2})$ hole states, respectively. In addition, a weak bump structure is observed at the location of the $1g_{7/2}$ hole state.

The proton-decay branching ratios to final states can be obtained from the ratio of the energy-integrated double-differential cross sections for coincidence with decay protons to final states and the singles cross section in the excitation energy range of 15.0–30.0 MeV. Such an analysis has been carried out for the three groups of final states of $^{207}$Tl corresponding to the $(3s_{1/2} + 2d_{3/2})$, $(1h_{11/2} + 2d_{5/2})$, and $1g_{7/2}$, as shown in Fig. 3. The singles double-differential cross sections were obtained from previous experimental results [7]. The partial branching ratios for proton decay obtained for these final states are listed in Table [II].

The errors quoted in the values of these branching ratios correspond only to the statistical uncertainties in the singles and coincidence double differential cross sections. Since the singles and coincidence measurements were performed with the same set-up and basically under identical conditions, the systematic errors would, in principle, cancel out in the ratios or, at any rate, be reduced greatly compared to the statistical errors. The total experimental
proton-decay branching ratio to the low-lying states of $^{207}$Tl is found to be $(1.97 \pm 0.3)\%$. The predictions of recent CRPA calculations for the partial branching ratios, $b_i$, for proton decay of the ISGDR in the excitation energy range 15.0–35.0 MeV in $^{208}$Pb to the $3s_{1/2}$, $2d_{5/2}$, $1h_{11/2}$, $2d_{5/2}$ and $1g_{7/2}$ hole states in $^{207}$Tl are also given in Table I, with a theoretical value totaling 2.51% \cite{18}. For comparison, the branching ratios from Ref. \cite{14} for direct proton decay of the ISGDR in the excitation energy range 19.0–25.0 MeV in $^{208}$Pb are provided as well.

### TABLE I: The experimental value of partial branching ratios (B. R.) for direct proton-decay from the ISGDR in the excitation-energy range of 15.5 MeV to 30.5 MeV in $^{208}$Pb to the various proton-hole states in $^{207}$Tl are given in percent. The theoretical branching ratios $b_i$ \cite{18}, which refer to the theoretical strength of ISGDR in the excitation-energy range of 15.0 MeV to 35.0 MeV, are also given. The values of branching ratios from previous work \cite{14} are provided for comparison.

| Final state | $E_{fs}$ (MeV) | $B.R_{\text{exp}}^a$ | $b_i^b$ | $B.R.^c$ |
|-------------|----------------|---------------------|--------|---------|
| $3s_{1/2}$  | 0.0            | 0.65%               |        |         |
|             |                | 0.74±0.15%          | 2.3±1.1% |         |
| $2d_{3/2}$  | 0.35           | 0.80%               |        |         |
| $1h_{11/2}$ | 1.35           | 0.29%               |        |         |
|             |                | 0.99±0.20%          | 1.2 ± 0.7% |         |
| $2d_{5/2}$  | 1.67           | 0.75%               |        |         |
| $1g_{7/2}$  | 3.47           | 0.24 ± 0.10%        | 0.02%  |         |

\textsuperscript{a}This work

\textsuperscript{b} Ref. \cite{18}

\textsuperscript{c}Ref. \cite{14} (see text)

In this work, we have employed the experimental singles differential cross section obtained from Ref. \cite{7} for extracting the branching ratios. In Ref. \cite{13}, on the other hand, the branching ratios could not be deduced directly because the corresponding singles cross sections for the ISGDR were not available. Instead, the partial differential cross sections for proton decay were converted directly to sum-rule strengths by comparison with the calculated DWBA
cross sections for 100% EWSR of the ISGDR located at the relevant excitation energy; these
sum-rule strengths were, then, stated as the branching ratios. This, of course, was subject
to the uncertainties associated with DWBA calculations, including also the uncertainty in
the centroid energy of the ISGDR. In a later analysis [14], the situation was rectified by
comparing the proton decay to specific states to the total decay cross section, including all
direct proton and neutron decays, and the statistical decays. The branching ratios included
in Table I are from Ref. [14] and are, essentially, equivalent to the true branching ratios
obtained in the present work. We find that while the branching ratios from the two mea-
measurements are in satisfactory agreement for the (1h11/2+2d5/2) hole states, there remains a
significant discrepancy for the (3s1/2+2d3/2) states. Also, the observed branching ratios are
in reasonable agreement with the CRPA predictions [18] except for the 1g7/2 state, where
the experimental branching ratio is larger by an order of magnitude.

Fig. 4(a) shows the double-differential cross section spectrum for θav=1.28°, corresponding
to the maximum of ISGDR cross section, and Fig. 4(b) for the forward angular range 0.0°–
0.3° (θav=0.19°). The subtraction spectrum is shown in Fig. 4(c) after taking into account
the excitation energy dependence of the transmission probabilities. While the statistics
in the subtraction spectrum are rather weak, it clearly shows the contribution from the
ISGDR component, as indicated by the solid line in Fig. 4(c), which is a Gaussian fit to
the data. The centroid energy of the ISGDR peak in the subtraction spectrum is 22.7±1.6
MeV which is in agreement with the value obtained in the singles measurement (22.7±0.2
MeV) [7]. It may be noted that, within the limited statistics of this experiment, there also are
bumps in the excitation-energy spectrum for θav=0.19° both above and below the ISGDR
region (see Fig. 4(b)). These bumps have been identified in the previous proton-decay measurements [13, 14] as corresponding, respectively, to L = 2 (the higher-lying bump) and
L = 3 excitation (the lower-lying bump). As mentioned earlier, and shown in Fig. 1, the
L=1 excitation cross section is significantly larger when compared with the L=2 excitation
cross section in the angular range 1.0° to 1.5° covered in our measurement. This might be a
reason why the L=2 strength above ISGDR region reported in the previous particle-decay measurement [13, 14, 15] is not seen as prominently in our data. Still, to get a quantitative
estimate of the L=2 contribution, the excitation energy spectrum in the range of 15.5–33.5
MeV was fitted with three Gaussian distributions. A free fit resulted in peaks with centroid
ergies of 17.2 MeV, 22.7 MeV, and 29.6 MeV, respectively, with the width of each peak
FIG. 4: (a) The double-differential cross section spectrum for the scattering angular range $\theta_{\text{c.m.}} = 1.0^\circ - 1.5^\circ$ and in the excitation-energy range -0.5 MeV < $^{207}\text{Tl}$ < 2.5 MeV. The solid lines are 3-Gaussian fits to the data (see text). (b) Same as (a) but for the scattering angular range $\theta_{\text{c.m.}} = 0.0^\circ - 0.3^\circ$. (c) The subtraction spectrum of (a) and (b). The subtraction spectrum clearly shows the contribution from the ISGDR component.

fixed at 3.8 MeV. That would put the “$L=2$” peak in our data at an energy slightly higher than that reported in Ref. [13]. It can be stated nonetheless that there exists some strength in our spectra at the location of the previously-reported $L=2$ peak. We have also carried out a three-peak fit by keeping the centroid energy of the middle peak fixed at 22.7 MeV and the other two centroid energies fixed at the values reported for the $L=2$ and $L=3$ peaks in Refs. [13, 14]; the resulting fit is shown in Fig. 4(a). The ratio of the integrated areas of the “$L=2$” Gaussian to the sum of the areas of the three Gaussian peaks suggests that the contribution of the $L=2$ multipole in the aforementioned excitation-energy range is around 22%, not inconsistent with the results of Refs. [13, 14], once the likely angular-distribution effects are taken into account.

In summary, the excitation and proton-decay of the ISGDR has been measured using the $^{208}\text{Pb}(\alpha, \alpha'p)^{207}\text{Tl}$ reaction at 400 MeV. The large ISGDR strength observed at the highest excitation energies that was observed in the singles measurements is not present in the
coincidence spectra, confirming the suggestion then advanced that this excess strength was spurious and arose from other, non-resonant, phenomena. The ISGDR centroid energy of $22.7 \pm 1.6$ MeV, obtained from the coincidence measurements, is in agreement with the value of $22.7 \pm 0.2$ MeV from the singles measurements. The total proton-decay branching ratio to low-lying states of $^{207}$Tl is found to be $(1.97 \pm 0.3)\%$, in reasonable agreement with the CRPA prediction of 2.51% for this value.

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