CAST solar axion search with $^3$He buffer gas: Closing the hot dark matter gap

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The CERN Axion Solar Telescope (CAST) has finished its search for solar axions with $^3$He buffer gas, covering the search range $0.64 \text{ eV} \lesssim m_a \lesssim 1.17 \text{ eV}$. This closes the gap to the cosmological hot dark matter limit and actually overlaps with it. From the absence of excess X-rays when the magnet was pointing to the Sun we set a typical upper limit on the axion-photon coupling $g_{a\gamma} \lesssim 3.3 \times 10^{-10} \text{ GeV}^{-1}$ at 95% CL, with the exact value depending on the pressure setting. Future direct solar axion searches will focus on increasing the sensitivity to smaller values of $g_{a\gamma}$, for example by the currently discussed next generation helioscope IAXO.

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Introduction.—The most promising method to search
For axions and axion-like particles (ALPs) \cite{11}, low-mass bosons with a two-photon interaction vertex, is their conversion to photons in macroscopic magnetic fields \cite{2, 3}. This approach includes the search for solar axions by the helioscope technique \cite{12, 13}, horizontal branch (HB) stars \cite{29} (a somewhat more restrictive limit stems from blue-loop suppression in massive stars \cite{30}), and the hot dark matter (HDM) bound \cite{31}. The yellow band represents typical theoretical models with \( |E/N| = 0 \) (KSVZ model).

One limiting factor in any of these efforts is the momentum difference between freely propagating photons and axions caused by the axion mass \( m_a \). It limits the magnetic field volume over which the conversion is coherent. In solar axion searches one can extend the search to larger \( m_a \) values by providing the photons with a refractive mass \cite{28}. The conversion pipe is filled with a low-\( Z \) buffer gas; the search mass is chosen by adjusting the gas pressure. In this way, the CERN Axion Solar Telescope (CAST), the largest axion helioscope to date, has successively pushed its search range to higher \( m_a \) values (see Fig. 1 for a summary of results). We here report on the final search range based on \( ^3\text{He} \) buffer gas.

Within the ALP family of hypothetical bosons, the original axion is the best-motivated case because it emerges from the compelling Peccei-Quinn mechanism to explain the absence of CP-violating effects in QCD. In the two-dimensional \( g_{a\gamma}-m_a \) ALP parameter space, the QCD axion must lie somewhere on a line \( g_{a\gamma} \propto m_a \).

The close relationship between axions and neutral pions implies that this line is anchored to the point describing the \( \pi^0 \) mass and the pion-photon coupling constant. After allowing for model-dependent numerical factors, the axion may be found anywhere in the yellow band indicated in Fig. 1. The CAST vacuum result \( g_{a\gamma} < 0.88 \times 10^{-10} \text{ GeV}^{-1} \) at 95% CL for \( m_a \lesssim 0.02 \text{ eV} \) \cite{13} remains a milestone in the ALP landscape. However, a major objective of CAST has been to find or exclude QCD axions and thus to push as far as possible to higher \( m_a \) values. Our first \( ^3\text{He} \) limits \cite{14} have for the first time crossed the axion line appropriate for the Kim, Shifman, Vainshtein, Zakharov (KSVZ) model (Fig. 1).

QCD axions with parameters in this range thermalize in the early universe after the QCD phase transition by interactions with pions \cite{34} and would thus exist with a present-day number density of around 50 cm\(^{-3}\), comparable to 0.5 neutrino species, and are therefore susceptible to hot dark matter bounds \cite{31, 35, 36}. Assuming neutrino masses to be negligible, the latest axion hot dark matter bound is \( m_a \lesssim 0.9 \text{ eV} \), leaving a small gap to our earlier \( ^3\text{He} \) search range which we now close.

The recent Planck measurements of the cosmic microwave background (CMB) significantly improve our knowledge of many cosmological parameters. In contrast to earlier CMB results, Planck alone now constrains the axion mass and provides a limit \( m_a < 1.01 \text{ eV} \) (95% CL) \cite{37}. The inclusion of other data sets, notably the matter power spectrum and the HST measurement of the Hubble parameter, have only a small impact, providing limits between 0.67 and 0.86 eV, depending on the combination of data sets \cite{58}. In other words, concerning a possible axion hot dark matter contribution to the universe, the situation after Planck is almost the same as before.

System description and data-taking strategy.—CAST uses a straight 10m LHC test dipole magnet (\( B \sim 9.0 \text{ T} \)), mounted on a movable platform to follow the Sun for about 1.5 h both at sunrise and sunset. The two bores extend beyond the cold mass (length 10.25 m) for 16 cm on each side forming 4 link regions which are closed by x-ray cold windows. The volume of the two cold bores is 30 L and the total volume of the link regions is 1.5 L. The magnetic field length of 9.26 m is centrally located within the cold mass. One of the apertures of the magnet is covered by a CCD/Telescope system \cite{38} and the other three by three Micromegas detectors of the microbulk type \cite{23, 24}. The axion-photon conversion probability when the conversion volume is filled with a buffer gas (\(^4\text{He} \) in our case) is \cite{14}

\[
P_{a\gamma} = \left( \frac{B g_{a\gamma}}{2} \right)^2 \frac{1 - e^{-\Gamma L} - 2e^{-\Gamma L/2} \cos(qL)}{q^2 + \Gamma^2/4}
\]

where the axion-photon momentum transfer provided by the magnetic field is \( q = |m_a^2 - m_{\chi}^2| / 2E \) and \( \Gamma \) is the inverse photon absorption length in the buffer gas. The
value of $\Gamma$ varies with the pressure and the energy, for example for a relatively high pressure of 70 mbar of $^3$He, for the mean energy of the expected flux of 4.3 keV, $\Gamma = 0.156 \text{ m}^{-1}$. The maximum conversion probability is reached for $m_a \simeq m_\gamma$, where $m_\gamma$ is the photon refraction mass which depends on the buffer gas density. For $m_a \neq m_\gamma$, the probability rapidly decreases due to the axion-photon momentum mismatch.

Throughout CAST Phase II, the data taking strategy was to increase the density in the cold bore circuit in small steps chosen to partially overlap the intrinsic mass acceptance ($\sim 1$ meV FWHM) of the previous setting and so scan smoothly over the whole available mass range. The original step size and exposure time have been modified on a number of occasions in order to complete the physics program more efficiently without compromising continuity, but at the expense of reduced sensitivity at higher masses.

The central gas density inside the cold bore, with the magnet horizontal, is calculated from the cold bore pressure ($P_{cb}$) measured at one end, the magnet temperature $T_{mag}$ and the equation of state (EoS) of $^3$He gas \[E_3\]. During solar tracking, $P_{cb}$ changes continuously, as expected, due to the changing hydrostatic pressure of the $^3$He gas column and due to a tilt-induced, slow characteristic temperature transient in the magnet (10–15 mK) from the cryogenic circuit. For example, at $P_{cb}$ 84 mbar, a vertical movement of the magnet of 6 degrees causes a shift in $P_{cb}$ of +1.06 mbar. Hydrostatic and magnet temperature effects account for +0.65 mbar. The remaining contribution of 0.4 mbar we ascribe to changing fluid dynamics in the buffer gas at the extremities of the cold bore.

The fluid dynamics effect is driven by the presence of short relatively warm link regions; the $^3$He temperature and density are not uniform throughout the whole system as regions with lighter vapor are present at the extremities, where buoyancy-driven flows occur. The magnet tilting affects such phenomena, giving rise to a redistribution of the $^3$He mass and a consequent pressure change. To take the pressure and temperature variation into account, our analysis procedure continuously calculates the density during solar tracking. First, the pressure in the center of the magnet is calculated from the $P_{cb}$ and the hydrostatic pressure difference. Then the density in the center is calculated from this central pressure and the temperature measurement (via the $^3$He EoS). In this way the fluid dynamics effects on the measured pressure directly change the central density value.

Although the $P_{cb}$ measurement allows us to calculate the central density at any moment, the actual density profile (which is needed to calculate the coherence length) and its variation on tilting cannot be measured directly and must be determined by Computational Fluid Dynamics (CFD) simulations. The CFD simulations take into account all requisite physical phenomena, such as gravity, natural convection and turbulence together with the geometry of the cold bores, link volumes and the cold windows and the buffer gas EoS. The boundary conditions are defined by $P_{cb}$, $T_{mag}$ and several temperatures measured around the link volumes and cold window flanges.

An extensive and on-going program of CFD simulations has been undertaken and CAST has made detailed studies with a number of different models to find the best description of the measured behavior. The tilted and horizontal cases were treated separately. Various turbulence models were used for the horizontal case and a model forcing laminar flow was favored, while a composite model was devised for the tilted case as the most intuitive natural description of the system. This model consists of a turbulent solution in the lower half of the cold bore smoothly joined to a laminar solution in the upper half. The predicted pressure variations between tilted simulations at different vertical angles are in satisfactory agreement with those observed experimentally (e.g. within 0.06 mbar for 84 mbar.)

For the analysis presented in this paper, the density profiles derived from turbulent CFD simulations made with the magnet horizontal and over the full range of Phase II density settings were subjected to a simple and conservative coherence criterion ($\Delta \rho < 0.001 \text{ kgm}^{-1}$). The resulting dependence of the effective coherence length $L_{eff}$ with density was parametrised and applied to all data independent of photon energy and tilt angle. $L_{eff}$ decreases from about ~9 m to ~6 m in the range $m_a$=0.4 eV to $m_a$=1.15 eV, compared with the magnetic length of 9.26 m. To estimate the systematic error of such an approach, an analysis was done using a coherence length $L_{eff}$ = 5.0 m for all angles and masses. This extreme case is only found in laminar horizontal simulations at the highest pressures. The final effect on the limit on the $g_{a\gamma}$ from applying this simple criterion is well below 10%.

Data analysis and results.—The results presented in this paper correspond to 1100 hour×detector taken by the three Micromegas detectors from 2009 to 2011 with $^3$He in the system in axion-sensitive conditions (i.e. with the magnet tracking the Sun). Background levels are determined from a larger body of data taken during non tracking time. The data acquired by the CCD/Telescope of this period is under analysis and will be presented in a later publication. The present data correspond to about 418 effective axion mass steps that, together with the first 252 $^3$He steps already released in a previous paper \[12\], continuously cover an axion mass range between 0.39 eV and 1.17 eV. Due to the density excursions experienced during a single tracking, data from each actual density step contribute to the neighbouring mass steps, especially for the larger densities used. The effective average exposure time per mass step is approximately 0.75 h per detector for masses from 0.64 eV to 1 eV, while it was reduced to ~0.4 h per detector for masses above 1 eV.

The data analysis is performed in a manner similar to our previous results \[12\] \[13\]. We use an unbinned likeli-
hhood function that can be expressed as

$$\log \mathcal{L} \propto -R_T + \sum_i^N \log R(t_i, E_i, d_i).$$

(2)

Here $R_T$ is the integrated expected number of counts over all exposure time, energy and detectors. The sum runs over each of the $N$ detected counts for the event rate $R(t_i, E_i, d_i)$ expected at the time $t_i$, energy $E_i$ and detector $d_i$ of the event $i$

$$R(t, E, d) = B_d + S(t, E, d),$$

(3)

where $B_d$ is the background rate of detector $d$. $S(t, E, d)$ is the expected rate from axions in detector $d$ which depends on the axion properties $g_{a\gamma}$ and $m_a$

$$S(t, E, d) = \frac{d\Phi_a}{dE} P_{a\rightarrow\gamma} \epsilon_d,$$

(4)

where $P_{a\rightarrow\gamma}$ is the axion photon conversion probability in the CAST magnet given by Eq. 1 and $\epsilon_d$ the detector effective area. Finally, the solar axion spectrum based on the Primakoff process is the same that was used in previous papers of this series [13]

$$\frac{d\Phi_a}{dE} = 6.02 \times 10^{10} g_{a\gamma}^2 \frac{E^{2.481}}{e^{E/1.205}} \text{ cm}^{-2} \text{s}^{-1} \text{keV}^{-1}$$

(5)

with $g_{10} = g_{a\gamma} / (10^{-10} \text{GeV}^{-1})$ and energies in keV. This result applies to axions with masses much smaller than the solar interior temperature, i.e., for sub-keV masses.

As explained in [14], the $m_a$ dependence of the above expression is encoded in the probability $P_{a\rightarrow\gamma}$, which is coherently enhanced for values of $m_a$ matching the refractive photon mass $m_\gamma$ induced by the buffer gas density, while it is negligible for values away from $m_\gamma$. Therefore, only the counts observed with the gas density matching a given axion mass $m_a$ will contribute to log $\mathcal{L}$ (and the exclusion plot) for that mass $m_a$. We stress that the value of $m_\gamma$ to be introduced is time-dependent even within a single density step, due to the pressure excursions explained above.

Maximization of $\mathcal{L}$ (for a fixed value of $m_a$) leads to a best-fit value of $g_{a\gamma}^{4\text{min}}$. The obtained value is compatible with the absence of a signal in the entire mass range, and therefore an upper limit on $g_{a\gamma}^4$ is obtained by integration of the Bayesian probability from zero up to 95% of its area in $g^4$. This is computed for many values of the axion mass $m_a$ in order to configure the full exclusion plot shown in Fig. 1. A close up of the same exclusion plot is shown in Fig. 2 focused specifically in the axion mass range which has been explored in the data presented here.

As can be seen in Fig. 1, CAST extends its previous range towards higher axion masses, excluding the interval 0.64–1.17 eV down to an average value of the axion-photon coupling of $3.3 \times 10^{-10} \text{GeV}^{-1}$. The actual limit contour has a high-frequency structure that is a result of statistical fluctuations that occur when a limit is computed for a specific mass using only a few hours of data. The green solid line corresponds to $E/N = 0$ (KSVZ model).

**FIG. 2:** Expanded view of the limit achieved in the CAST $^3$He phase for the axion mass range between 0.64 eV and 1.17 eV, which corresponds to a pressure scan in $^3$He from 36 mbar to 105 mbar approximately. The actual limit contour has a high-frequency structure that is a result of statistical fluctuations that occur when a limit is computed for a specific mass using only a few hours of data. The apparent slope upwards in the exclusion line for higher axion masses is due to the reduction of the exposure time per density step, for $m_a > 1$ eV, as well as to the continuous decrease of $L_{\text{eff}}$ and the increase of $\Gamma$ for higher gas densities. Eventually, with the addition of the data from the CCD/Telescope system, these numbers will likely improve.

**Conclusions.**—CAST has finished its phase of using $^3$He buffer gas, continuing the search to its limiting pressure setting corresponding to a search mass of $m_a = 1.17$ eV. In this way, the search range now generously overlaps with the current cosmic hot dark matter bound of $m_a \sim 0.9$ eV and there would be little benefit in pushing to yet larger masses with the buffer-gas technique. CAST has not found axions and the next challenge is to move down in the $m_a$–$g_{a\gamma}$ plot to reach the “axion band” of theoretical models in a broader range of masses. Such a goal cannot be achieved with the existing CAST apparatus and will require significant improvements of detector and magnet properties, such as the proposed International AXion Observatory (IAXO) [44, 45] or a completely new approach.

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[1] J. Jaeckel and A. Ringwald, Ann. Rev. Nucl. Part. Sci. 60, 405 (2010).
[2] A. Ringwald, Phys. Dark Univ. 1, 116 (2012).
[3] J. L. Hewett et al., arXiv:1205.2671
[4] P. Brun, arXiv:1304.1330
[5] P. Sikivie, Phys. Rev. Lett. 51, 1415 (1983); (E) ibid. 52, 695 (1984).
[6] G. Raffelt and L. Stodolsky, Phys. Rev. D 37, 1237 (1988).
[7] S. J. Asztalos et al., Ann. Rev. Nucl. Part. Sci. 56, 293 (2006).
[8] D. M. Lazarus et al., Phys. Rev. Lett. 69, 2333 (1992).
[9] S. Moriyama et al., Phys. Lett. B 343, 147 (1998).
[10] Y. Inoue et al., Phys. Lett. B 536, 18 (2002).
[11] Y. Inoue et al., Phys. Lett. B 668, 93 (2008).
[12] K. Zioutas et al. (CAST Collaboration), Phys. Rev. Lett. 94, 121301 (2005).
[13] S. Andriamonje et al. (CAST Collaboration), JCAP 0704, 010 (2007).
[14] E. Arik et al. (CAST Collaboration), JCAP 0902, 008 (2009).
[15] M. Arik et al. (CAST Collaboration), Phys. Rev. Lett. 107, 261302 (2011).
[16] K. Van Bibber, N. R. Dagdeviren, S. E. Koonin, A. K. Kerman and H. N. Nelson, Phys. Rev. Lett. 59, 759 (1987).
[17] J. Redondo, A. Ringwald and, Contemp. Phys. 52, 211 (2011).
[18] R. Bähre et al., arXiv:1302.5647
[19] A. Payez, J. R. Cudell and D. Hutsemekers, JCAP 1207, 041 (2012).
[20] A. De Angelis, G. Galanti and M. Roncadelli, Phys. Rev. D 84, 105030 (2011).
[21] D. Horns, L. Maccione, M. Meyer, A. Mirizzi, D. Montanino and M. Roncadelli, Phys. Rev. D 86, 075024 (2012).
[22] M. Meyer, D. Horns and M. Raue, Phys. Rev. D 87, 035027 (2013).
[23] S. J. Asztalos et al. (ADMX Collaboration), Phys. Rev. Lett. 104, 041301 (2010).
[24] J. Hoskins et al., Phys. Rev. D 84, 121302 (2011).
[25] S. J. Asztalos et al., Nucl. Instrum. Meth. A 656, 39 (2011).
[26] O. K. Baker et al., Phys. Rev. D 85, 035018 (2012).
[27] D. Horns et al., JCAP 1304, 016 (2013).
[28] K. van Bibber, P. M. McIntyre, D. E. Morris and G. G. Raffelt, Phys. Rev. D 39, 2089 (1989).
[29] G. G. Raffelt, Lect. Notes Phys. 741, 51 (2008).
[30] A. Friedland, M. Giannotti and M. Wise, Phys. Rev. Lett. 110, 061101 (2013).
[31] S. Hannestad, A. Mirizzi, G. G. Raffelt and Y. Y. Y. Wong, JCAP 1008, 001 (2010).
[32] J. E. Kim, Phys. Rev. Lett. 43, 103 (1979).
[33] M. A. Shifman, A. I. Vainshtein and V. I. Zakharov, Nucl. Phys. B 166, 493 (1980).
[34] S. Chang and K. Choi, Phys. Lett. B 316, 51 (1993).
[35] S. Hannestad, A. Mirizzi and G. Raffelt, JCAP 0507, 002 (2005).
[36] A. Melchiorri, O. Mena and A. Slosar, Phys. Rev. D 76, 041303 (2007).
[37] M. Archidiacono, S. Hannestad, A. Mirizzi, G. Raffelt and Y. Y. Y. Wong, arXiv:1307.0615
[38] M. Kuster et al., New J. Phys. 9, 169 (2007).
[39] P. Abbon et al., New J. Phys. 9, 170 (2007).
[40] S. Andriamonje et al., JINST 5, P02001 (2010).
[41] J. Galan et al., JINST 5, P01009 (2010).
[42] S. Aune et al. (CAST Collaboration), Nucl. Instrum. Meth. A 604, 15 (2009).
[43] E. W. Lemmon (NIST), private communication.
[44] I. G. Iristorza et al., JCAP 1106, 013 (2011).
[45] I. Shilon, A. Dudarev, H. Silva and H. H. J. ten Kate, IEEE T Appl. Supercon. 23, 3, p. 4500604 (2013).