Low-frequency observations of the giant radio galaxy NGC 6251

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ABSTRACT

We present LOFAR observations at 150 MHz of the borderline FRI/FRII giant radio galaxy NGC 6251. This paper presents the most sensitive and highest resolution images of NGC 6251 at these frequencies to date, revealing for the first time a low-surface-brightness extension to the northern lobe, and a possible backflow associated with the southern lobe. The integrated spectra of components of NGC 6251 are consistent with previous measurements at higher frequencies, similar to results from other LOFAR studies of nearby radio galaxies. We find the outer structures of NGC 6251 to be either at equipartition or slightly electron dominated, similar to those of FRII sources rather than FRIs, but this conclusion remains tentative because of uncertainties associated with the geometry and the extrapolation of X-ray measurements to determine the external pressure distribution on the scale of the outer lobes. We place lower limits on the ages of the extension of the northern lobe and the backflow of the southern lobe of \( t \gtrsim 250 \text{ Myr} \) and \( t \gtrsim 210 \text{ Myr} \), respectively. We present the first detection of polarization at 150 MHz in NGC 6251. Taking advantage of the high Faraday resolution of LOFAR, we place an upper limit on the magnetic field in the group of \( B_\leq 0.2 (\Lambda_B/10 \text{kpc})^{-0.5} \mu \text{G} \) for a coherence scale of \( \Lambda_B \leq 60 \text{kpc} \) and \( B < 13 \mu \text{G} \) for \( \Lambda_B = 240 \text{kpc} \).

Key words: polarization – galaxies: active – radio continuum: galaxies.

1 INTRODUCTION

Giant radio galaxies (GRGs) are a population of radio galaxies with projected linear sizes greater than 1 Mpc (Willis, Strom & Wilson 1974). These sources are typically found in galaxy groups and in terms of their Fanaroff–Riley (FR) classification (Fanaroff &
The origin of the Mpc sizes of GRGs has been investigated by many authors (Saripalli et al. 1997; Mack et al. 1998; Machalski, Chyży & Jamrozy 2004; Subrahmanyan et al. 2008; Komber & Pashchenko 2009). GRGs are not thought to be intrinsically different from the more common smaller radio galaxies but rather a later stage in their evolution (Machalski & Jamrozy 2006; Jamrozy et al. 2008; Komber & Pashchenko 2009). Machalski & Jamrozy argue that the correlation between the degree of depolarization and the linear size suggests that the environments of GRGs also play a role in their formation. X-ray observations of the intergalactic medium (IGM) of some GRGs combined with optical spectroscopic observations of the group galaxies show that the X-ray luminosity of the IGM is much lower, by as much as an order of magnitude, than would be expected from the correlation between X-ray luminosity and velocity dispersion (Chen et al. 2011, 2012), suggesting that the density of the environment is quite low. However, Komber & Pashchenko note that GRGs can be found in a range of environments ranging from very poor groups to clusters.

In many cases, the lobes of GRGs appear to extend beyond their host environment into the large-scale structure (LSS) of the Universe. Many GRGs exhibit asymmetries in their source structure, which may reflect asymmetries in their host environments (Schoenmakers et al. 2000; Lara et al. 2001; Pirya et al. 2012). Pirya et al. find that the shorter jet/lobe tends to be directed towards overdensities of galaxies. The lobes of GRGs are potentially powerful indirect probes of the warm hot intergalactic medium (WHIM) that exists in large-scale filaments. The WHIM is a natural prediction of ΛCDM cosmology and is thought to contain ~50 per cent of the baryonic matter in the Universe (Davé et al. 2001; Nicastro, Mathur & Elvis 2008; Smith et al. 2011). Recent Sunyaev–Zeldovich studies claim to have detected this low-density material for the first time (de Graaff et al. 2019; Tanimura et al. 2019). Indirect measurements of the WHIM using observations of GRGs provide an important complementary tool to trace this material, by assuming that the lobes of GRGs are relaxed and in equilibrium with the external WHIM pressure. By calculating the internal pressure of the lobe, we can therefore measure the pressure in the WHIM (Subrahmanyan et al. 2008; Safouris et al. 2009). Malairecki et al. (2015) combine radio observations of GRGs with spectroscopic optical observations of nearby galaxies to demonstrate that it is possible to use GRGs to probe the denser regions of the WHIM.

In order to calculate the internal pressure of the GRG lobe, it is necessary to make some assumptions about the particle energetics. The simplest assumption one can make when calculating the internal pressure is that the relativistic electrons and magnetic field are in equipartition, with equal energy density (e.g. Hardcastle et al. 2002; Laing & Bridle 2002; Croston et al. 2004). This assumption can be tested for radio galaxies in those cases where X-ray observations are able to detect the intra-cluster medium or the inverse-Compton radiation of the lobes. Such comparisons have been carried out for many sources. In general, it is found that FRII sources are close to equipartition, with high-energy electrons only slightly dominating over the energy of the magnetic field (e.g. Brunetti et al. 1999; Hardcastle & Worrall 2000; Croston et al. 2005; Migliori et al. 2007; Isobe & Koyama 2015; Kawakatu, Kino & Takahara 2016; Ineson et al. 2017). In contrast, for FRI sources it is typically found that equipartition implies them to be significantly underpressured, with a significant violation of equipartition required for them to match the pressure of their surroundings (Morganti et al. 1988; Worrall & Birkinshaw 2000; Croston et al. 2008; Croston & Hardcastle 2014). The apparent difference in FRI and FRII particle content/energetics is discussed in detail by Croston, Ineson & Hardcastle (2018).

Past studies attempting to constrain the energetics in radio galaxies were limited by the lack of low-frequency observations. The lobes of radio galaxies generally have steep spectra, and any variation from the assumed spectral behaviour at low frequencies could lead to large changes in the calculated energetics. With the advent of new low-frequency instruments, such as the LOw Frequency ARray (LOFAR; van Haarlem et al. 2013), the recently upgraded Giant Meterwave Radio Telescope (GMRT uGMR T; Swarp 1991; Gupta et al. 2017), and the Murchison Widefield Array (MWA; Tingay et al. 2013), we can now begin to constrain the behaviour of the low-energy electron population. Indeed, recently Harwood et al. (2016) demonstrated that, in the case of FRII sources, the low-frequency spectra can be steeper than previously assumed, leading to an increase in the estimated total energy content of the lobes, as large as a factor of 5 in the case of 3C 452.

In this paper, we present total-intensity and polarized-intensity observations of the nearby GRG NGC 6251 at 150 MHz with LOFAR high-band antennas (HBA). NGC 6251 is a GRG with a projected linear size of 1.7 Mpc (Perley et al. 1984) and a borderline FRI/FRII morphology. The main jet and lobe are centred-brightened like an FRI; however, there is a hotspot or ‘warm spot’ in the northern lobe suggestive of an FRII. In contrast, the southern jet/lobe structure is edge-brightened, but possesses an inner hotspot somewhat reminiscent of wide-angle tail structures. The radio power at 178 MHz is \( P_{178} \approx 1.4 \times 10^{25} \text{W Hz}^{-1} \) (Waggett, Warner & Baldwin 1977), within an order of magnitude of the traditional Fanaroff & Riley (1974) division between FRI and FRII sources (~10^{25} W Hz\(^{-1}\) in our assumed cosmology; see below) – although note that this division is now known to be more blurred, and potentially strongly environmentally dependent (e.g. Mingo et al. 2019). The large-scale morphology of NGC 6251 has some similarities with sources previously classed as ‘hybrids’, but now thought to be strongly projected sources with FRI-like jets (Harwood, Vernstrom & Stroe 2020); it is likely that projection as well as an intermediate jet power and environmental effects together explain the unusual structure.

There have been many radio observations of NGC 6251. The first observations were carried out by Waggett et al. (1977) at 150 MHz and 1.4 GHz. Perley et al. (1984) present detailed high-resolution Very Large Array (VLA) observations of the main jet in NGC 6251 at 1.4 GHz. Mack et al. (1997a, 1998) present observations of the large-scale structure of NGC 6251 from 325 MHz to 10 GHz. Observations also show that NGC 6251 is highly linearly polarized, as much as 70 per cent in some regions, which is close to the theoretical maximum (Stoffel & Wielebinski 1978; Willis, Wilson & Strom 1978; Saunders et al. 1981; Perley et al. 1984; Mack et al. 1997a).

X-ray observations have revealed an X-ray jet, as well as extended emission from the group-scale environment (Mack, Kerp & Klein 1997b; Evans et al. 2005). Evans et al. also used these observations to investigate the internal conditions in the lobes (but see the discussion in Section 4.1.1). There have also been gamma-ray
observations of NGC 6251: the Fermi team reported detections of NGC 6251 as 1FGL J1635.4+8228 in the first-year Fermi catalogue (Abdo et al. 2010) and as 2FGL J1629.4+8236 in their second-year catalogue (Nolan et al. 2012). The 95 per cent error on the position of 2FGL J1629.4+8236 includes both the jet and lobe of NGC 6251. Takeuchi et al. (2012) observed NGC 6251 with Suzaku and detected diffuse X-ray emission in its northern lobe. They argue that 2FGL J1629.4+8236 is consistent with non-thermal inverse-Compton emission from the lobes, based on detailed modelling of the spectral energy distribution (SED).

The aims of the work presented in this paper are twofold. Our first aim is to investigate the low-frequency radio-continuum spectral behaviour of NGC 6251 and re-examine the pressure balance in its lobes, taking into account the new LOFAR data. Our second aim is to probe the environment and source structure using the high-resolution Faraday spectra obtained using the LOFAR HBA data. The material in this paper is split between Section 2, in which we describe the observational data and its basic processing, Section 3, in which we derive results regarding spectra and polarization, Section 4, in which we discuss these results with reference to the above aims, and Section 5, in which we summarize our conclusions.

A preliminary report of this work has been previously published (Cantwell 2018), and contains additional details of some intermediate results that are omitted here for clarity. This paper, with the benefit of peer review, confirms the main conclusions of the preliminary report, but more rigorously defines the conditions under which they are valid, and extends them: in particular, it extends the scope of this work to include this effect directly during calibration. This leads to a significant increase in noise for the weighted average \( \bar{X} = \frac{\sum_i a_i^2 X_i}{\sum_i a_i^2} \), where \( X_i \) is the image in band \( i \) and \( \sigma_{\text{rms,i}} \) is the root-mean-square (rms) noise. The effective frequency for this weighted average is 140 MHz, though throughout the rest of this document we label these data with the nominal 150 MHz mid-frequency for this LOFAR band. Fig. 1 shows the full field of view, and Fig. 2 shows a zoomed-in image of NGC 6251. The expected thermal noise with these parameters is approximately 0.2 mJy beam\(^{-1}\), while the measured noise in our images is 2 mJy beam\(^{-1}\). This increase in noise is typical for data which, like ours, have not undergone direction-dependent calibration (van Weeren et al. 2016).

### 2.1 LOFAR

#### 2.1.1 Calibration and imaging

An initial flagging step was performed using AOFLAGGER (Offringa, van de Gronde & Roerdink 2012).1 3C 295 was then calibrated using BlackBoard SelfCal (BBS) and a simple two-component model. The flux scale was set using Scaife & Heald (2012). These solutions were transferred to the target and then a phase-only self-calibration was performed on each sub-band using the LOFAR global sky model (gsm) (Smirnov & Noordam 2004). The data were imaged with AWIMAGER (Tasse et al. 2013) to generate a new sky model, which was then used to perform a single round of phase-only self-calibration. The data were combined into 18 bands of 3.515 MHz each with a channel width of 48 kHz. We did not carry out direction-dependent calibration (e.g. van Weeren et al. 2016), as our primary target was the bright central source, and the image quality achievable with a direction-independent calibration was sufficient for our science aims.

Final imaging was carried out using AWIMAGER using Briggs weighting with a robustness parameter of 0. Due to issues with radio-frequency interference (RFI), only 63 MHz of the 80 MHz total bandwidth was used. In order to investigate the diffuse emission, each band was imaged separately, with an outer \( \lambda/\Omega \) limit of 3k\( \lambda \) in units of wavelength \( \lambda \), achieving a resolution of 40 arcsec. At this point, the flux scale was corrected as described in Section 2.1.2. The flux-corrected images were combined to produce a weighted average \( \bar{X} = \frac{\sum_i a_i^2 X_i}{\sum_i a_i^2} \), where \( X_i \) is the image in band \( i \) and \( \sigma_{\text{rms,i}} \) is its root-mean-square (rms) noise. The effective frequency for this weighted average is 140 MHz, though throughout the rest of this document we label these data with the nominal 150 MHz mid-frequency for this LOFAR band. Fig. 1 shows the full field of view, and Fig. 2 shows a zoomed-in image of NGC 6251. The expected thermal noise with these parameters is approximately 0.2 mJy beam\(^{-1}\), while the measured noise in our images is 2 mJy beam\(^{-1}\). This increase in noise is typical for data which, like ours, have not undergone direction-dependent calibration (van Weeren et al. 2016).

#### 2.1.2 Flux-density scale

There are known problems with the LOFAR HBA flux-density scale (Heald et al. 2015; Hardcastle et al. 2016). As with any aperture array, the LOFAR primary beam is elevation dependent, leading to different primary beams when observing the calibrator source and the target source. This difference should be accounted for when transferring the amplitude gains from the calibrator source to the target field. However, as the overall normalization of the LOFAR HBA beam is poorly constrained, it is not currently possible to include this effect directly during calibration. This leads to a frequency-dependent effect on the LOFAR HBA fluxes. In order to correct for this effect, we follow the flux boot-strapping procedure outlined by Hardcastle et al. (2016).2

First, a catalogue of sources was generated for our LOFAR field using PYBDSF.3 From this catalogue, bright sources with fluxes \( > 0.1 \text{Jy} \) were cross-matched with the VLA Low-Frequency Sky Survey (VLSSr; Lane et al. 2012) and the NRAO VLA Sky

1. https://sourceforge.net/projects/aoflagger
2. https://github.com/mhardcastle/lofar-bootstrap
3. PYBDSF documentation: http://www.astron.nl/citt/pybdsf/
survey (NVSS; Condon et al. 1998). The final catalogue of sources contained only those with sources having both a VLSSr counterpart and an NVSS counterpart. A flux correction factor was then found for each band and applied to the LOFAR field, and a new source catalogue for the field was generated.

To test the reliability of this flux correction, we found the spectral index for every source within the half-power distance of the LOFAR primary beam with an NVSS counterpart. The spectral indices of these sources have a mean of $-0.8$ and standard deviation of 0.3. This is consistent with our expectation, suggesting that our corrected flux scale is reliable.

2.1.3 Polarization imaging

The commissioning of a pipeline to process LOFAR polarization data is not yet complete, and so it is not currently possible to calibrate the instrumental polarization and thus to determine the absolute polarization angle. However, it is still possible to detect polarized emission with LOFAR (Mulcahy et al. 2014; O’Sullivan et al. 2019), and science commissioning has shown that linearly polarized intensity and Faraday-depth values can be reliably recovered for known polarized sources. The Faraday depth is defined as

$$\phi = 0.81 \int n_e B \cdot dl \ \text{rad} \ m^{-2},$$

where $n_e$ is the electron density in cm$^{-3}$, $B$ is the magnetic field in $\mu$G, and $dl$ is the path-length in parsec.

To image polarized emission from NGC 6251, we must account for Faraday rotation due to the ionosphere, which results, per equation (1), from ionospheric free electrons and the geomagnetic field. Variations in the ionospheric electron content and the projection angle of the geomagnetic field during the observations will lead to different degrees of Faraday rotation throughout the data, causing a smearing of any signal in Faraday space (Sotomayor-Beltran et al. 2013). We corrected for ionospheric Faraday rotation with RMEXTRACT$^4$ (Mevius 2018), which calculates the expected Faraday rotation over the LOFAR stations from a model of the geomagnetic field and maps of the ionospheric total electron content (TEC). The geomagnetic field is taken from the International Geomagnetic Reference Field (IGRF), and the TEC maps may be obtained from either the Centre for Orbital Determination in Europe (CODE)$^5$ or the Royal Observatory of Belgium (ROB)$^6$. Tests during commissioning investigating pulsars of known properties suggest that using CODE ionospheric maps recovers more of the true polarized flux, and so we used these as the input for the ionospheric correction (Van Eck 2017). CODE calculates the TEC using data from $\sim200$ GPS and Global Navigation Satellite System (GLONASS) sites of the International GPS Service (IGS) and other institutions, with a time resolution of about an hour, and a spatial resolution of $2.5^\circ \times 5.0^\circ$ (Dow, Neilan & Rizos 2009). Fig. 3 shows a

$^4$https://github.com/maaijke/RMExtract
$^5$http://aiuws.unibe.ch/ionosphere/
$^6$http://gnss.be/Atmospheric_Maps/ionospheric_maps.php
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Figure 2. Contours and grey-scale image showing the LOFAR 150 MHz HBA total-intensity map of NGC 6251. Contours are shown at $-3, 3, 5, 10, 15, 20, 60, 150, 200, 400 \times \sigma_{\text{rms}}$, where $\sigma_{\text{rms}} = 2.0 \text{ mJy beam}^{-1}$. The blue circle in the bottom left-hand corner shows the beam resolution. Radial artefacts are visible around background sources to the north-west and south-west, but fall below the first contour threshold well before they reach the northern lobe of NGC 6251, so we do not expect them to appreciably affect our results.

Figure 3. Faraday rotation due to the ionosphere. There is a single outlier visible in the plot, which was excluded from our analysis.

plot of the ionospheric rotation-measure (RM) correction produced by RMExtract.

Once the RM correction had been applied to every sub-band and time-step, individual channels of 48 kHz were split from sub-bands and imaged in Stokes Q and U using AWIMAGER. An inner $uv$ limit of 200λ, corresponding to an angular scale of $\sim 20$ arcmin, was used in order to avoid imaging Galactic foreground emission.

2.2 Archival data

We have used a number of archival data sets in our analysis of NGC 6251. We have used the Westerbork Synthesis Radio Telescope (WSRT) 325 and 610 MHz images as well as the Effelsberg 10 GHz images from Mack et al. (1997a), which are discussed in detail in that work and by Mack et al. (1998). A number of VLA data sets from the archive were also used; the details of these are summarized in Table 2. The VLA data sets used were chosen to best match the resolution of the LOFAR observations. Observations at 8 GHz in D configuration as well as 1.4 GHz and 325 MHz in B configuration were used to image the core of NGC 6251.
Table 2. Details of archival VLA data used in this work, including the configuration of the telescope at the time of the observations, the frequency used, and the reference for the image based on the data.

| Proposal ID | Date       | Configuration | Frequency | Reference                |
|-------------|------------|---------------|-----------|--------------------------|
| AK461       | 1998 Oct 5 | B             | 325 MHz   | This work                |
| VJ49,VJ38   | 1988 Nov 20| A,B           | 1.4 GHz   | Evans et al. (2005)     |
| Test        | 1985 Dec 5 | D             | 1.4 GHz   | This work                |
| AB3346      | 1985 Dec 1 | D             | 1.4 GHz   | This work                |
| AM0322      | 1991 May 9 | D             | 8 GHz     | Evans et al. (2005)     |

Figure 4. Northern lobe of NGC 6251. Grey-scale shows the VLA 1.4 GHz D-configuration image, with contours in red at $-\frac{5}{3}, \frac{3}{3}, 5, 10, 20, 30, 40, 100 \times \sigma_{\text{rms}}$, where $\sigma_{\text{rms}} = 1.0 \text{ mJy beam}^{-1}$. LOFAR 150 MHz HBA contours are shown in blue at $3\sigma_{\text{rms}}$, where $\sigma_{\text{rms}} = 2.0 \text{ mJy beam}^{-1}$. The blue circle in the bottom left-hand corner shows the VLA beam resolution.

Figure 5. Southern lobe of NGC 6251. VLA 1.4 GHz D-configuration and LOFAR 150 MHz HBA data are shown as in Fig. 4.

Observations at 1.4 GHz in D configuration were used to analyse the large-scale structure of NGC 6251.

The B-configuration 325 MHz data and D-configuration 1.4 GHz data were imaged and reduced in CASA 4.7 (McMullin et al. 2007). A simple calibration strategy was adopted for the D-configuration 1.4 GHz data. The flux scale was that of Perley & Butler (2013). An initial phase calibration was performed using the flux calibrator followed by the bandpass calibration and a final amplitude and phase calibration. NGC 6251 was observed as two pointings: one centred on the core and the other on the southern lobe. Both pointings were imaged in two steps. In the first round of imaging we applied a mask that excluded large extended regions, and did not carry out multiscale cleaning. Once all compact emission or narrow emission, such as the jet, was included in the model, a second round of imaging was carried out using multi-scale CLEAN, in order to properly image the diffuse emission. The data were imaged with a $uv$ range of 140–4400, and natural weighting. The final images of the northern and southern lobes are shown in Figs 4 and 5, respectively.

The VLA 325 MHz data were calibrated similarly, with one additional step at the start of the procedure. Data from the Global Positioning System (GPS) were used to generate a map of the ionospheric electron content, and a phase correction based on this map was applied to the data using the CASA task gencal. The resulting image is shown in Fig. 6. The resolution and rms noise of this and the other images used in this paper are summarized in Table 3.

3 RESULTS

The full-bandwidth LOFAR image of NGC 6251 is shown in Fig. 2. The main jet extends north-west from the core, with a bright knot at a distance of 200 arcsec (or 99.6 kpc in projection). The jet then bends north, and terminates at a hotspot. The northern lobe overlaps with the hotspot and jet down as far as the knot, but a diffuse, low-surface-brightness component extends west from the lobe. This extension was detected in the 325 MHz map of Mack et al. (1997a);
however, the 150 MHz LOFAR data presented here show that the region extends at least a further 14.4 arcmin (or 430 kpc), so that the total length of the faint extension is 19 arcmin (or 581 kpc).

The counterjet is detected at a 3σ level in the LOFAR image shown in Fig. 2, which is the clearest detection of the counterjet at these frequencies to date. The counterjet extends to the south-east. At 700 arcsec (or 349 kpc in projection) from the core, the jet bends to the east. The bend is bright and detected at 325 MHz, 610 MHz, and 1.4 GHz. The VLA 1.4 GHz image in Fig. 5 shows that the brightened jet continues eastward in a linear fashion until it reaches a bright, compact hotspot. The jet is again deflected at the hotspot and continues to the south-east before terminating in a well-defined southern lobe.

A region of diffuse low-surface-brightness emission can be seen coincident with the southern jet. This emission was previously only seen in the 150 MHz map of Waggett et al. (1977). As such this appears to be very steep-spectrum emission, and may originate in lobe material that has been deflected back towards the core. We henceforth refer to this region as the ‘southern backflow’; for further discussion, see Section 4.1.2.

Table 4 shows the flux densities measured within the 3σ contour line for individual components of NGC 6251, for a range of frequencies between 150 MHz and 10 GHz. Fig. 7 shows a map of the regions used to define the components. Point sources embedded in the lobe emission were replaced with blanked pixels. Errors in the flux measurements were calculated using the equation

$$
\sigma_S = \sqrt{(\sigma_{cal} S_n)^2 + (\sigma_{\text{rms}} \sqrt{N_{\text{beam}}})^2},
$$

where $N_{\text{beam}}$ is the number of independent beams in the region and $\sigma_{\text{cal}}$ is the fractional uncertainty in the calibration of the flux-scale, which we take to be 10 per cent. For the southern jet, we placed 3σ upper limits on the flux density at 325 MHz, 610 MHz, and 1.4 GHz assuming the surface brightness at these frequencies to be uniform over the region in which the jet was detected in the 150 MHz image. We placed similar limits at 325 MHz and 610 MHz for the northern extension, but not at 1.4 GHz, as the VLA 1.4 GHz data did not cover this area.

### 3.1 Spectral index

The integrated spectral index was calculated for each component of NGC 6251 using the fluxes shown in Table 4. Fig. 8 shows the best-fitting power law for the spectrum of each component and Table 4 lists the fitted spectral indices. It should be noted that the $uv$ range of the interferometric maps used to measure the flux densities are not matched as we did not have access to the $uv$ data for all the images. This could lead to an artificial steepening of the measured spectral index in regions of diffuse extended emission such as the lobes.

The core of NGC 6251 cannot be separated from the inner jet region in the LOFAR, WSRT, or low-resolution 1.4 GHz images. The flux from the core contributes to the inner jet region. In order to subtract the core contribution from the inner jet region, archival 325 MHz, 1.4 GHz, and 8 GHz VLA data were used. Table 4 shows the core fluxes measured from each of these data sets. The spectral index of the core as measured from these data is inverted and has a value of $\alpha = +0.3 \pm 0.1$. Using this spectral index, the core flux was predicted for each of our data sets and subtracted from the integrated flux of the inner jet region.

To investigate the variation of the spectral index across the source and reduce the ambiguity associated with inconsistent $uv$ coverage, the LOFAR data were re-imaged with a $uv$ range of 140–4400 $\lambda$, matching that of the VLA. This ensures that both total-intensity maps used to calculate the spectral index include emission from the same spatial scales, although they may still differ in the $uv$ coverage of the specific observations. The resulting LOFAR image has an rms of 1.5 mJy beam$^{-1}$. A spectral-index map was made from 150 MHz to 1.4 GHz using pixels exceeding a 7σ limit. The resulting images are shown in Figs 9 and 10. Due to the inner $uv$ limit at 140 $\lambda$, neither the extension nor the southern backflow are visible in the $uv$-matched LOFAR image.

The spectral-index map in Fig. 9 shows the core of NGC 6251 to have a flat spectrum. The spectral index is around −0.5 along the axis of the inner part of the main jet, steepening on either side. The jet steepens as it enters the northern lobe to −0.7, before flattening to around −0.5 in the hotspot. The spectral index of the northern lobe varies from around −0.7 near the jet and hotspot to ≤−1 towards the western extension.

The western extension of the northern lobe is outside the primary beam of the VLA. The shortest baseline for the WSRT is 36 m that gives a maximum angular scale of 47 arcmin at 610 MHz and 88 arcmin at 325 MHz. The WSRT data should therefore be sensitive to emission on these scales. The fact that the LOFAR image shows the extension continuing for another 14.4 arcmin past what is seen in the WSRT 325 MHz image suggests that the emission has a very steep spectral index, at least steeper than $\alpha = −2.7$. The emitting electrons are likely very old.

The base of the southern counterjet can also be seen in Fig. 9. The spectral index is $<−0.6$, steeper than in the main jet. This appears to be the flattest part of the pre-bend region of the counterjet. Beyond 60 kpc, the counterjet has steepened such that it is only visible at 150 MHz.

The counterjet reappears at higher frequencies in what appears to be a bend (see Fig. 10). The spectral index of this bend is around −0.5 with a cocoon of steeper emission ($\alpha < −0.9$) surrounding it. The spectral index for the southern hotspot is almost flat, with $\alpha > −0.5$. Similar to the extension of the northern lobe, the diffuse low-surface-brightness emission seen around the southern jet in the LOFAR image is not seen in the 325 MHz WSRT image, suggesting...
Table 4. Measured flux densities and limits for individual components of NGC 6251 at various frequencies from 150 MHz to 10 GHz, and fitted spectral indices $\alpha$ (see Section 3.1). Flux-density data are from the images listed in Table 3, except for the 8 GHz value, which is from Evans et al. (2005).

| Component          | $S_{150\text{MHz}}$ | $S_{325\text{MHz}}$ | $S_{610\text{MHz}}$ | $S_{1.4\text{GHz}}$ | $S_{8\text{GHz}}$ | $S_{10\text{GHz}}$ | $\alpha$   |
|--------------------|---------------------|---------------------|---------------------|---------------------|-------------------|-------------------|------------|
| Core region        | 0.2 ± 0.1$^a$       | 0.27 ± 0.04$^b$     | 0.32 ± 0.07$^b$     | 0.4 ± 0.1           | 0.72 ± 0.03       | 0.8 ± 0.3$^a$    | 0.3 ± 0.1  |
| Inner jet (core incl.) | 2.2 ± 0.2          | 1.4 ± 0.1           | 1.2 ± 0.1           | 0.9 ± 0.1           | –                 | 0.81 ± 0.08      | –          |
| Inner jet (core excl.) | 1.9 ± 0.2          | 1.2 ± 0.1           | 0.9 ± 0.1           | 0.5 ± 0.1           | –                 | 0.1 ± 0.3        | −0.6 ± 0.2  |
| Knot               | 2.8 ± 0.3           | 1.7 ± 0.2           | 1.2 ± 0.1           | 0.75 ± 0.08         | –                 | 0.22 ± 0.02      | −0.60 ± 0.07 |
| Outer jet          | 1.8 ± 0.2           | 0.90 ± 0.09         | 0.56 ± 0.06         | 0.34 ± 0.04         | –                 | 0.072 ± 0.0008   | −0.75 ± 0.08 |
| Northern lobe      | 6 ± 1               | 2.0 ± 0.5           | 1.0 ± 0.3           | 0.5 ± 0.1           | –                 | –                 | −1.1 ± 0.3  |
| Northern extension | 2.6 ± 0.3           | <0.32               | <0.28               | –                   | –                 | –                 | −2.7$^c$   |
| Northern hotspot   | 2.0 ± 0.2           | 0.93 ± 0.09         | 0.59 ± 0.06         | 0.35 ± 0.04         | –                 | 0.083 ± 0.0009   | −0.73 ± 0.08 |
| Southern jet       | 0.26 ± 0.03         | <0.09               | <0.08               | <0.03               | –                 | –                 | −1.4$^c$   |
| Southern backflow  | 1.8 ± 0.2           | <0.169              | <0.1                | 0.05 ± 0.01         | –                 | –                 | −1.6 ± 0.2  |
| Southern lobe      | 5.8 ± 0.6           | 1.5 ± 0.2           | 0.51 ± 0.05         | 0.44 ± 0.06         | –                 | –                 | −1.3 ± 0.2  |
| Southern hotspot   | 1.0 ± 0.1           | 0.30 ± 0.03         | 0.20 ± 0.02         | 0.15 ± 0.02         | –                 | 0.022 ± 0.003    | −0.85 ± 0.09 |

Notes. $^a$Predicted using core spectral index calculated from VLA 325 MHz, 1.4 GHz, and 8 GHz data. $^b$Measured from VLA 325 MHz data rather than the WSRT image at the same frequency. $^c$Limit calculated from LOFAR 150 MHz flux density and WSRT upper limits at 325 and 610 MHz.

Figure 7. Illustration of the regions we define for each component of NGC 6251 used to integrate intensities to obtain flux densities for those components. Contours shown are a subset of those in the LOFAR 150 MHz image in Fig. 2.

that the spectral index is at least as steep as $-1.6$. This is steeper than the spectral index seen in the lobe, suggesting that this is ageing material from the lobe being redirected back along the jet axis.

There are substantial discrepancies between the spectral-index map of the southern region of the source in Fig. 10(a) and the steeper integrated spectral indices derived from Fig. 8(b) and listed in Table 4. These may result from inconsistent $uv$ coverage: Fig. 10(a) shows spectral indices based only on our $uv$-matched total-intensity maps, whereas the integrated spectral indices also incorporate the maps of Mack et al. (1997a). They may also result from differences in the assumed location of the emission: the integrated spectral indices are based on the regions defined in Fig. 7 including the

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Figure 8. Integrated spectra and power-law fits for each component of NGC 6251, as defined in Fig. 7, except the core region. Fluxes are arbitrarily scaled to fit on the plot. Note that the emission from the southern backflow is likely to come from multiple components, e.g. jet emission contributes at 1.4 GHz. Similarly, several points at 1.4 GHz may include confusion noise from the bright core, which would explain the unusual convex spectra. Dashed lines represent upper limits on the spectrum calculated from the LOFAR data and WSRT 325 MHz $3\sigma$ upper limits.

Figure 9. (a) Spectral-index maps between 150 MHz and 1.4 GHz for the northern lobe of NGC 6251. The flux cut-off used was $7\sigma_{\text{rms}}$ where $\sigma_{\text{rms}} = 1.5 \text{ mJy beam}^{-1}$ is the rms noise of the LOFAR image. (b) Corresponding spectral-index error map.

Figure 10. (a) Spectral-index maps between 150 MHz and 1.4 GHz for the southern lobe of NGC 6251, with the same flux cut-off as in Fig. 9(a). Note that the colour scale differs from Fig. 9(a). (b) Corresponding spectral-index error map.
fringes of the lobe, which fall below the flux cut-off used for the spectral-index maps and might be expected to have systematically older, steeper emission.

3.2 Polarization

The Stokes Q/U images produced per Section 2.1.3 were analysed with both RM synthesis (Section 3.2.1) and QU fitting (Section 3.2.2).

3.2.1 Rotation-measure synthesis

RM synthesis (Brentjens & de Bruyn 2005) involves direct calculation of the Faraday spectrum from Stokes Q/U data. It is computationally efficient, and not dependent on specific model assumptions, but the output can be misleading when there are multiple Faraday structures along the line of sight (Farnsworth, Rudnick & Brown 2011), and it is subject to limitations in scale and resolution for any realistic finite bandwidth. The maximum observable Faraday depth, $\phi_{\text{max-depth}}$, the resolution in Faraday space, $\delta\phi$, and the largest scale in Faraday space that can be detected, $\phi_{\text{max-scale}}$, are (Brentjens & de Bruyn 2005)

\[
\|\phi_{\text{max-depth}}\| \approx \sqrt{3} \frac{\lambda^2}{\Delta \lambda^2},
\]

\[
\delta\phi \approx \frac{2\sqrt{3}}{\Delta \lambda^2},
\]

\[
\phi_{\text{max-scale}} \approx \frac{\pi}{\lambda_{\text{min}}}.
\]

where $\Delta \lambda^2$ is the width of a channel in $\lambda^2$, $\Delta \lambda^2$ is the total width of the $\lambda^2$ coverage, and $\lambda_{\text{min}}$ is the minimum value of $\lambda^2$. For our observations, this gives $|\phi_{\text{max-depth}}| \approx 677 \text{ rad m}^{-2}$, $\delta\phi \approx 0.87 \text{ rad m}^{-2}$, and $\phi_{\text{max-scale}} \approx 0.46 \text{ rad m}^{-2}$.

We calculated the Faraday spectrum from the Stokes Q and U images, neglecting spectral dependence of the polarized flux, using the RM synthesis code PyRMSynth. In our first iteration, we searched the entire range of Faraday depths to which our observations were sensitive, from $-1000$ to $+1000 \text{ rad m}^{-2}$, using a coarse Faraday-depth cell size of $2 \text{ rad m}^{-2}$. From this spectrum, we excluded any structure at large Faraday depths. In our second iteration, we searched over Faraday depths from $-300$ to $+300 \text{ rad m}^{-2}$ with a cell size of $0.2 \text{ rad m}^{-2}$ to properly sample the rotation measure spread function (RMSF). Fig. 11 shows the RMSF of the LOFAR data.

Following Van Eck et al. (2018), we fit a Rayleigh distribution to the Faraday spectrum of each pixel in order to estimate the noise in the Faraday spectra. Faraday depths between $-20$ and $+20 \text{ rad m}^{-2}$ were masked to avoid fitting the instrumental polarization. The scale parameter $\sigma$ was assumed to be the noise in the spectrum. An $8\sigma$ detection threshold was applied to the spectrum of each pixel.

Fig. 12 illustrates typical Faraday spectra from both an unpolarized field source and a polarized region of NGC 6251. Faraday spectra like these, calculated per Section 3.2 for each pixel in the image, constitute a Faraday cube. Fig. 13 shows the polarized intensity at the maximum in the Faraday spectrum for each pixel, after excluding the region $-15 \text{ rad m}^{-2} < \phi < +15 \text{ rad m}^{-2}$ to exclude the instrumental polarization. The blue contours mark the regions where the peak in the Faraday spectrum is $>8\sigma_{\text{rms}}$.

\[\text{https://github.com/mrbell/pyrmsynth}\]
Low-frequency observations of NGC 6251

Figure 13. Polarization in the northern lobe of NGC 6251. Grey-scale shows peak polarization in the Faraday depth cube, with blue contours at 8σ. Red contours show unpolarized emission in the same LOFAR data at 3, 5, 10, 15, 20 × σrms, where σrms = 2.0 mJy beam−1. Faraday spectra for representative pixels in the polarization-detected knot and lobe are shown in Fig. 14.

where σrms is the noise in the Faraday spectrum of that pixel. There is a clear detection of polarization in the knot of the jet, with peak intensity at 16h30.5m 82°33.3′, as well as some patchy structure in the northern lobe. The rest of the source is depolarized.

Fig. 14 shows the Faraday spectrum for a representative pixel in the knot and a representative pixel in the lobe. The Faraday spectrum of the lobe shows a single Faraday-thin component. The average Faraday depth of this component for the pixels in which a polarization detection has been made is −54.1 rad m−2 with a standard deviation of 0.4 rad m−2. The mean amplitude of the Faraday-thin component in the lobe is 1.8 ± 0.1 mJy beam−1 RMSF−1.

The knot shows a single Faraday-thin component with an average Faraday depth of −50.97 rad m−2 and a standard deviation of 0.07 rad m−2. The average amplitude of this component is 3 mJy beam−1 RMSF−1 with a standard deviation of 1 mJy beam−1 RMSF−1. The fractional polarization is approximately 1 per cent. Perley et al. (1984) report typical polarization fractions in the jet of ∼10 per cent at 1662 MHz, rising to a peak ∼40 per cent around the position of the knot (their fig. 15). Our lower polarization fraction may result from a combination of beam depolarization due to variation in the polarization angle across the jet (their fig. 17), and our inclusion of unpolarized emission from the steeper-spectrum emission on either side of the jet, due to both our lower frequency and our larger beam size.

Perley et al. (1984) also report polarized emission at 1662 MHz with a polarization fraction ∼20 per cent from the inner jet, which does not appear in Fig. 13. This may be caused by Faraday depolarization, either inherent to the source or resulting from the group environment, which would suppress the polarized signal at our lower frequency of 150 MHz. Note that Perley et al. measure strong RM gradients in this region (see their Fig. 20a).

3.2.2 QU fitting

QU fitting involves fitting parameters of a modelled polarized source to reproduce observed Stokes Q/U data. A model for the polarized intensity \( P(\lambda^2) = Q + iU \) of a Faraday-thin source can be expressed as

\[
P(\lambda^2) = p_0 \exp[2i(\chi + \phi \lambda^2)].
\]

where \( \chi \) is the polarization angle and \( p_0 \) is the initial polarized intensity. More complex models can be constructed e.g. from the superposition of multiple such sources. QU fitting typically achieves more precise reconstruction of source parameters (including Faraday depth) than RM synthesis (Sun et al. 2015), but is dependent on selection of the correct model, and is more computationally intensive. Here, we use QU fitting as a follow-up to further investigate the structure of the polarized emission described in Section 3.2.1 and to more precisely reconstruct its Faraday depth. We use the QU-JB code presented by Sun et al. (2015), which explores the parameter space and evaluates Bayesian evidence using the MultiNest library (Feroz & Hobson 2008; Feroz, Hobson & Bridges 2009; Feroz et al. 2019).

We fitted a number of different models to our data. First, our null hypothesis was that only instrumental polarization is present, which we modelled as a first-order polynomial in frequency space. This order was chosen as it was sufficient to adequately suppress the instrumental polarization, while insufficient to fit out or degrade an astronomical signal at significantly non-zero Faraday depth. We
then fitted a series of models with both this instrumental polarization and one, two, or three Faraday-thin components, each with a contribution to the polarized emission as given in equation (4), approximated to be independent of frequency over our band. We did not fit for any models with Faraday-thick components, as LOFAR HBA is minimally sensitive to these: from equation (3c), the maximum scale recoverable is $\phi_{\text{max-scale}} = 0.46 \text{ rad m}^{-2}$, so any polarized source with Faraday thickness exceeding this would not be properly recovered, although the edges in its Faraday spectrum might be visible if they were sufficiently sharp (Van Eck et al. 2017).

In order to evaluate the quality of the fits across the knot and the lobe we calculate for each pair of models the Bayes factor, $K$, which is given by

$$K = \frac{\Pr(D | M_2)}{\Pr(D | M_1)} = \frac{\int \Pr(\theta_1 | M_2) \Pr(D | \theta_1, M_2) d\theta_1}{\int \Pr(\theta_1 | M_1) \Pr(D | \theta_1, M_1) d\theta_1}, \quad (5)$$

where each model $M_i$ is defined in terms of parameters $\theta_i$, is assigned a prior $\Pr(\theta_i | M_i)$, fits the data with likelihood $\Pr(D | \theta_i, M_i)$, and is supported by Bayesian evidence $\Pr(D | M_i)$. Following Kass & Raftery (1995), we evaluate the Bayes factor based on the derived value $2\ln K$: a positive value supports model 2, constituting weak evidence. Negative values of $2\ln K$ show the evidence of the models with two or three Faraday-thin components, each with a variance in the Faraday depth is $\sigma = 0.7 \text{ rad m}^{-2}$, in agreement with that measured from the Faraday spectra, with amounts as a function of time (Van Eck et al. 2017). This leads to a wide posterior distribution. However, for the structure to be real, the estimated errors would need to be three times larger than the actual uncertainty in Faraday depth.

4 DISCUSSION AND ANALYSIS

4.1 Spectral index and energetics

The spectral-index maps of NGC 6251 presented in Section 3.1 are the first to extend down to 150 MHz at this angular resolution, permitting detailed modelling of the electron populations responsible for this emission. In this section, we perform this modelling to determine the pressure, age, and energetics of electrons in the lobes of NGC 6251, and discuss these results with reference to the literature.

As a check, we compare our 150 MHz–1.4 GHz spectral-index maps presented here to the 325–610 MHz and 408 MHz–10 GHz maps of Mack et al. (1998). We find that our map agrees well with their 325–610 MHz map except for the bend in the southern jet. Here, we find a spectral index of $\alpha = -0.5$, whereas Mack et al. find $\alpha = -1$. The 150 MHz LOFAR image shown in Fig. 2 shows the backflow of the lobe material from the southern lobe. In the 325 MHz WSRT image only a small region of this structure is detected and in the 610 MHz image only the bend is visible. We suggest that the presence of the older lobe emission, coincident with the jet, has led to the steep spectral index in the Mack et al. spectral-index map and that the bend is indeed a real feature of the counterjet.

4.1.1 Internal pressure and magnetic field

The internal pressure of a relativistic plasma can be calculated from its energy density, with contributions from relativistic electrons ($U_e$), protons ($U_p$), and the magnetic field ($U_B$). Assuming equipartition between the magnetic field and the relativistic particles, and defining the ratio $k = U_e/U_B$, which we take to be constant, then the internal pressure is

$$P_{\text{int}} = \frac{k + 2}{3} U_B. \quad (7)$$

We calculate $U_e$ and $U_B$ using the SYNCH code (Hardcastle, Birkinshaw & Worrall 1998), with the spectral indices from Section 3.1 as inputs. Briefly, this code calculates the energetics of a relativistic plasma in equipartition, given a measurement of the radio flux, the proton/electron energy-density ratio $k$, and a power-law model of the electron energy distribution, including minimum and maximum energies of the population and, optionally, a spectral break. From these, it calculates the equipartition magnetic field strength, and hence the energy density of the magnetic field and electron population.

We applied SYNCH to find $U_B$ under these assumptions for each component of NGC 6251. We assumed protons to be absent ($k = 0$) and took the low-energy and high-energy cut-offs for the electron population to be, respectively, $5 \times 10^4$ and $5 \times 10^{11} \text{ eV}$. The low-energy value corresponds to a minimum Lorentz factor, below which synchrotron losses are unimportant, of $\gamma_{\text{min}} = 10$. Investigations of hotspots suggest values of $\gamma_{\text{min}} \sim 10^2$ (Barai & Wita 2006), or typical values around $10^2$ with occasional values up to $10^4$, but we expect the minimum Lorentz factors in lobes to be lower than in hotspots due to adiabatic expansion. Within this energy range, we assumed an injection index of $p = -0.6$, consistent with the synchrotron spectral index $\alpha = (p - 1)/2 \sim -0.8$ in the hotspots and main jet, with a break energy at which the spectrum steepens to

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the observed spectral index for other components. With the energy range fixed, we found the available radio data were best fit with a break energy of $1 \times 10^9$ eV. Finally, we assumed a spherical, elliptical, or cylindrical volume for each component as seemed appropriate based on the LOFAR image.

Our assumptions and the resulting fitted pressure for each component are shown in Table 5. As the northern extension and southern backflow are likely populated by a very old population of electrons, with limited spectral information available, these data were fitted assuming high-energy cut-offs chosen for consistency with the 325 MHz radio limit, which were $1 \times 10^{10}$ eV for the backflow and $2 \times 10^9$ eV for the extension.

In Fig. 17, we compare the calculated internal pressure with the external pressure as measured from thermal X-ray observations (Evans et al. 2005). As the volumes we calculate are highly uncertain for components containing unresolved emission, we restrict this figure, and our discussion below, to the lobes and their corresponding extension/backflow, for which the volumes are better defined. The external pressures derived from X-ray observations are constrained only out to 150 kpc, beyond which we extrapolate using a two-component $\beta$ model (Croston et al. 2008). We find that, assuming equipartition, the northern lobe is underpressured by a factor of $\sim 2$ and its extension overpressured by a factor of $\sim 10$, while the southern lobe is overpressured by a factor of $\sim 10$ and its backflow underpressured by a factor of $\sim 1.7$. We note that the internal, equipartition pressure of the western lobe reported by Evans et al. (2005) and reproduced by Croston et al. (2008) appears to be too low, due to an incorrect low-frequency flux measurement used by those authors.

If projection effects are taken into account, both northern and southern lobes may be further from the group centre than their projected distances, placing them in a lower-pressure environment and thus giving them higher pressures relative to their surroundings. The northern lobe, underpressured by a factor of $\sim 330$ kpc, would be at pressure balance under equipartition assumptions if its true position were $\sim 440$ kpc from the group centre. This would place it on the axis of a straight jet at an angle to the line of sight of 41 deg, or more or less than this if the jet bends, which appears likely. The southern lobe, overpressured at its projected distance of $\sim 1000$ kpc, would be more strongly overpressured if it is projected out of the plane of the sky.

Projection effects also come into play when calculating the volume of the lobes. Evans et al. (2005) argue that the axis of the northern lobe is close to the plane of the sky based on an observed discontinuity in the X-ray surface brightness, in which case projection effects will have a minimal impact on its volume. The southern lobe, however, could be substantially larger than we have calculated if it is elongated along the line of sight. To take an extreme case, if it were a cylinder with a length of 1000 kpc aligned along the line of sight, it would have an increased volume of $7.9 \times 10^{66}$ m$^3$ and a decreased pressure of $2 \times 10^{-15}$ Pa, leaving it overpressured only by a factor of 4.

Another source of uncertainty is our assumption that $\gamma_{\text{min}} = 10$. To test the dependence of our results on this value, we have rerun the calculations assuming $\gamma_{\text{min}} = 1$ and $\gamma_{\text{min}} = 10^3$ for the northern lobe and southern lobe. Lower values of $\gamma_{\text{min}}$ imply higher values for the internal pressure, and vice versa. The northern lobe, which is underpressured by a factor of 2 in our default case, is underpressured
The areas with the steepest spectral indices in NGC 6251 are the extension of the northern lobe and the region between the core and the southern lobe, which we have referred to as a backflow. This label is motivated by the implied age of the material: if it has passed through the southern lobe and is flowing back towards the group centre, this would explain why its implied age is greater than that of the lobe proper. One could also, however, construct a model in which this region contains material directly from the southern jet that has been deposited before the formation of the current southern lobe.

As these steep-spectrum components – the northern extension and the southern backflow – are clearly detected only at 150 MHz, we cannot fit for a break frequency; we instead assume that this frequency $\nu_b$ lies somewhere below 325 MHz. We calculate the age $t$ of both components following Alexander & Leahy (1987) so that

$$t = \frac{1590}{\sqrt{\nu_b(1+z)^2} \left( \frac{B}{\mu G} \right) 0.5},$$

where $B = 3.18(1+z^2)^2$ is the equivalent field strength of the cosmic microwave background radiation assuming the present-day temperature of 2.726 K. Using the equipartition magnetic fields in Table 5 (see Section 4.1.1), this places lower limits of $t \gtrsim 250$ Myr for the age of the northern extension and $t \gtrsim 210$ Myr for the southern backflow. The data for both the northern and southern

### Table 5. Parameters for the calculation and evaluation of the internal pressure $P_{\text{int}}$ for each component of NGC 6251 (see Section 4.1.1). Each component is defined in Fig. 7, and its apparent shape in this image is used to calculate its volume, from which we determine the equipartition magnetic field $B_{\text{eq}}$ and internal pressure $P_{\text{int}}$. The external pressure $P_{\text{ext}}$ is as measured at the projected distance of each component; the ratio $P_{\text{ext}}/P_{\text{int}}$ indicates whether the component is under- or overpressured.

| Component                      | Shape       | Volume ($\times 10^{64}$) | $B_{\text{eq}}$ ($\mu$G) | $P_{\text{int}}$ (Pa) | $P_{\text{ext}}$ (Pa) | $P_{\text{ext}}/P_{\text{int}}$ |
|-------------------------------|-------------|---------------------------|--------------------------|-----------------------|-----------------------|----------------------------------|
| Core region                   | –           | –                         | –                        | –                     | –                     | –                                |
| Inner jet (core subtracted)   | Cylindrical | $1.07 \times 10^{64}$     | 2.5                      | $1.7 \times 10^{-14}$ | $4.8 \times 10^{-13}$ | 28                               |
| Knot                          | Cylindrical | $4.88 \times 10^{63}$     | 3.5                      | $3.3 \times 10^{-14}$ | $1.2 \times 10^{-13}$ | 4                                |
| Outer jet                     | Cylindrical | $9.84 \times 10^{63}$     | 2.7                      | $1.9 \times 10^{-14}$ | $2.4 \times 10^{-14}$ | 1.2                              |
| Northern lobe                 | Spherical   | $1.55 \times 10^{66}$     | 1.2                      | $3.7 \times 10^{-15}$ | $7.9 \times 10^{-15}$ | 2                                |
| Northern extension            | Cylindrical | $9.1 \times 10^{65}$      | 1.4                      | $4.9 \times 10^{-15}$ | $4.9 \times 10^{-16}$ | 0.1                              |
| Northern hotspot              | Ellipsoid   | $5.43 \times 10^{63}$     | 3.2                      | $2.7 \times 10^{-14}$ | $3.4 \times 10^{-15}$ | 0.1                              |
| Southern jet                  | Cylindrical | $3.24 \times 10^{64}$     | 1.0                      | $3.4 \times 10^{-15}$ | $5.2 \times 10^{-14}$ | 15                               |
| Southern backflow             | Cylindrical | $1.29 \times 10^{65}$     | 0.8                      | $1.6 \times 10^{-15}$ | $2.8 \times 10^{-15}$ | 1.7                              |
| Southern lobe                 | Spherical   | $1.32 \times 10^{66}$     | 1.3                      | $4.8 \times 10^{-15}$ | $4.9 \times 10^{-16}$ | 0.1                              |
| Southern hotspot              | Ellipsoid   | $7.09 \times 10^{63}$     | 2.6                      | $1.8 \times 10^{-14}$ | $9.5 \times 10^{-16}$ | 0.05                             |

### Figure 17. Internal and external pressures for NGC 6251 over a range of distances from its core. The solid black line shows the external pressure calculated from the thermal X-ray emission, with uncertainty shaded grey, and the hatched region showing an extrapolation where there is no direct observation of the environment. (a) Internal pressure of the northern lobe and corresponding extension, compared with a value calculated from inverse-Compton (IC) measurements (Takeuchi et al. 2012). (b) Internal pressure of the southern lobe and southern backflow.
lobes show no sign of a break. Taking 10 GHz as a lower limit for the break frequency we find that the ages of both the northern and southern lobes have an upper limit of $t \lesssim 40$ Myr.

### 4.1.3 Group environment

The north–south asymmetry found for the lobes of NGC 6251 in Section 4.1.1, with the northern and southern lobes, respectively, marginally under-pressured and significantly over-pressured at equipartition, might be explained by invoking asymmetry in the group environment. If the large-scale atmosphere is not symmetric about NGC 6251 as we have assumed, but the external pressure profile instead flattens at large radii around the southern lobe only, the southern lobe might instead be much closer to pressure balance. It has been suggested that the asymmetries seen in radio galaxies are due to environmental effects (Schoenmakers et al. 2000; Lara et al. 2004; Firy et al. 2012). The southern jet in NGC 6251 terminates 2.2 times further from the core than the northern jet. Chen et al. (2011) show that the galaxy overdensity is larger in the direction of the shorter main jet of NGC 6251. There is therefore reason to believe the environment of NGC 6251 could be asymmetric. However, the current available X-ray data is not sufficient to investigate this directly.

A separate estimate of the particle energetics comes from observations of inverse-Compton emission. Takeuchi et al. (2012) fit a model to radio, X-ray and gamma-ray data. They find the combined data are best fitted with a magnetic field in the lobe of $B = 0.37 \mu$G (approximately three times smaller than the equipartition magnetic field calculated in Section 4.1.1) and an injection spectral index of $\alpha = -0.5$, which breaks to $\alpha = -0.75$ at $E_\text{b} = 1.5 \times 10^9$ eV. This gives an energy ratio of $U_r/U_b = 45$ and an internal pressure of $8.5 \times 10^{-15}$ Pa. This would place the lobe in pressure balance with the external environment at the projected distance of the lobe from the cluster centre. The region used to calculate this pressure includes both the lobe and the hotspot. Given that the electron population in the hotspot and the lobe would be expected to have different characteristics, the pressure calculated by Takeuchi et al. is likely to be an overestimate, and so it seems likely that the true internal pressure may be somewhere between the equipartition pressures calculated in this paper and by Takeuchi et al.

The northern extension and southern backflow are the oldest components in NGC 6251. As such, while it is possible that the lobes are somewhat overpressured, the extended tail-like regions of the extension and backflow are more likely to be in equilibrium with the environment. The host galaxy group has an estimated $r_{200}$ of 875 kpc (Croston et al. 2008). The northern lobe reaches a projected distance of $\sim r_{500}$, while the southern lobe reaches beyond $r_{200}$. The extended structure of NGC 6251 is therefore probing the outskirts of the group environment and the large-scale structure beyond. The internal pressure of the extension, if at equipartition with no significant proton contribution, implies an environmental pressure of $4.9 \times 10^{-15}$ Pa, and the internal pressure of the southern backflow implies an environmental pressure of $1.6 \times 10^{-15}$ Pa. Malarecki et al. (2015) find similar pressures for 12 GRGs, and show that this pressure corresponds to the densest 6 per cent of the WHIM.

### 4.2 Polarization analysis

The detection of polarized emission at low frequencies such as the 150 MHz observations presented in this work is an effective means to precisely reconstruct Faraday depths, which has driven a great deal of recent activity. Mulcahy et al. (2014) presented the first detections of extragalactic polarization with LOFAR using RM synthesis and found approximately 1 source per 1.7 deg$^2$. Orrù et al. (2015) also report the detection of polarization in the outer lobes of the double–double radio galaxy B1834+620. Van Eck et al. (2018) published a catalogue of 92 polarized sources at 150 MHz in the LOFAR Two-meter Sky Survey (LOTSS) preliminary data release region. Polarized sources have also been detected at these frequencies with the MWA: Rilesey et al. (2018) published a catalogue of 81 polarized sources in the POLarized GLEAM Survey (POGS) corresponding to $\sim 1$ source per 79 deg$^2$.

Our results in Section 3.2 show polarized emission in the region of the bright knot in the main jet, as well as a small region of patchy polarization in the northern lobe. All polarization in the inner part of the jet is depolarized, due to RM gradients in this region (Perley et al. 1984). It is likely that the majority of the Faraday rotation observed is due to our Galaxy, but estimating the exact value of this contribution is difficult. Higher-frequency, high-resolution data presented by Perley et al. (their fig. 20b) show that beyond 180 arcsec (89 kpc) from the core the average Faraday depth is $-48.9 \pm 0.2$ rad m$^{-2}$, which they suggest to be the Galactic contribution. Oppermann et al. (2015) reconstruct a map of the Galactic Faraday contribution using observations of extragalactic sources. This reconstructed map has an average Faraday rotation of $-31.6$ rad m$^{-2}$ in the region of NGC 6251. These values suggest that the extragalactic contribution is of order 1–10 rad m$^{-2}$.

The Faraday-depth values we measure in the knot are in good agreement with those found by Perley et al. (1984). Due to LOFAR’s high resolution in Faraday space, it is possible to confirm that the Faraday depth is truly flat in this region with an average of $-50.97$ rad m$^{-2}$ and a standard deviation of 0.07 rad m$^{-2}$. This corresponds to the bright knot region in the LOFAR images and is the only strong detection of polarization in our LOFAR HBA observations of NGC 6251.

#### 4.2.1 Limit on the group magnetic field

The detection of Faraday-thin polarized emission in the knot in the main jet and at a point in the northern lobe constitutes two measurements of the structure function, or the variation in Faraday depth as a function of physical scale. The detection of continuous Faraday-thin emission with a variance of $\sigma_{\text{RM}}^2 = 5 \times 10^{-3}$ rad$^2$ m$^{-4}$ (see Section 3.2.2) across the knot, which has a size of 2 arcmin or 60 kpc in projection, is a measurement of the structure function at scales up to this value. Similarly, the difference in Faraday depth of $\delta_{\text{RM}} = 2.8$ rad m$^{-2}$ between the knot and the lobe gives us a single realization of the structure function at a scale equal to their separation, which is 8 arcmin or 240 kpc in projection.

The measured variance of the Faraday depth in each case constitutes an upper limit on the variance $\sigma_{\text{RM}}^2$ that results from Faraday rotation in turbulent magnetic fields in the group environment, thus allowing us to place an upper limit on the strength of these magnetic fields. If the group environment is assumed to be composed of cells each with a uniform density and magnetic field strength but with a random field orientation then the expected variance in Faraday depth is

$$\sigma_{\text{RM}}^2 = \left( \frac{e^3}{8\pi^2 e_0 m_e^2 c^3} \right)^2 \Lambda_B \int \left( B_1 n_e \right)^2 dl, \quad (9)$$

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where $\varepsilon_0$ is the vacuum permittivity, $c$ is the speed of light, and $e$ and $m_e$ are the charge and mass of the electron, or
\[
\sigma_{\text{DM}}^2 = \left(812 \text{ rad m}^{-2}\right)^2 \frac{\Lambda_B}{\text{ kpc}} \int \left(\frac{B_1}{\mu\text{G cm}^{-3}}\right)^2 \frac{d\ell}{\text{kpc}},
\]
(10)
where $B_1 = B / \sqrt{3}$ is the component of the magnetic field along the line of sight and $\Lambda_B$ is the size of the cells, related to the characteristic coherence length of the magnetic field (Lawler & Dennison 1982; Govoni et al. 2010).

Assuming $B$ in the group environment to be constant, the integral in equation (10) reduces to $\int n_e^2 dl$; i.e. we need to know how the electron density $n_e$ varies along the line of sight. For this purpose, we use a profile of $n_e$ for the group derived from X-ray observations (Croston et al. 2008, their equation 1 and table 4), taking it to be centred on the core of NGC 6251, and integrate along the line of sight from specific positions in this profile. For the Faraday-depth variation in the knot – assuming the jet to be at an angle of $\sim 40^\circ$ to the line of sight, based on the jet/counter-jet ratio (Jones & Wehrle 2002; Perley et al. 1984) – we find the knot to be separated from the core by 150 kpc in the plane of the sky and an additional 200 kpc towards us along the line of sight and integrate from this point. For the difference in Faraday depth between the knot and the polarization-detected region of the lobe, we take a point mid-way between them, separated from the core by 250 kpc in the plane of the sky and 330 kpc towards us along the line of sight. Note that these points are beyond the X-ray observations used to produce the fitted profile, which has a maximum scale radius of 150 kpc: we are extrapolating the profile slightly outside of its fitted range, as in Fig. 17.

Under these assumptions, from equation (10), we find that the Faraday-depth variation in the knot implies a limit $B < 0.2(\Lambda_B/10\text{kpc})^{-0.5} \mu\text{G}$ on the magnetic field in the group environment at scales $\Lambda_B < 60$ kpc. For the difference $\delta_{\text{RM}}$ in Faraday depth between the knot and the lobe, as this constitutes only a single realization of the magnetic turbulence, we use equation (10) with $\sigma_{\text{DM}}^2 = \delta_{\text{RM}}^2$, but relax the resulting limit by a factor of 2, permitting a 95 per cent confidence limit against a Gaussian distribution, which gives us $B < 13 \mu\text{G}$ at the specific coherence-length scale $\Lambda_B = 240$ kpc. In practice, the model described by equation (10), with magnetic-field structure at only a single scale, will not be a full description of the group environment, and a more detailed model may allow the above limits to be violated by a factor $\sim 2$ (their section 5.7 and fig. 16 of Laing et al. 2008b).

These magnetic-field limits may be compared to previous calculations for NGC 315, another GRG in a similarly sparse environment to NGC 6251. Laing et al. (2006) find residual fluctuations in the Faraday depth of NGC 315 of order 1–2 rad m$^{-2}$ and suggest that, for plausible assumptions for the central density and characteristic magnetic field length, the central magnetic field would have to be $B_0 = 0.15 \mu\text{G}$. This is comparable to the upper limit calculated here for NGC 6251 for coherence lengths $\Lambda_B \sim 20$ kpc. Denser group environments such as those of 3C 449 and 3C 31 have central magnetic field strengths of order a few $\mu\text{G}$ (Laing et al. 2008a; Guidetti et al. 2010), but field strength is expected to decrease with radius.

5 CONCLUSIONS
In this paper, we have presented new observations of NGC 6251 at 150 MHz with LOFAR HBA. The images presented here are the highest sensitivity and resolution images of NGC 6251 at these frequencies to date and reveal both an extension to the northern tail and backflow extending from the southern lobe towards the nucleus. The integrated low-frequency spectral index is consistent with that measured previously at higher frequencies. The lobes of NGC 6251 appear to be either close to equipartition or slightly electron dominated, similar to FRII sources; however, the lack of well-determined external environmental pressure measurements, and the uncertain and asymmetric large-scale geometry, mean that this conclusion is tentative. We place lower limits on the ages of the low-surface-brightness extension of the northern lobe and the backflow of the southern lobe, which we have detected for the first time and are only visible at these low frequencies, of $t \gtrsim 250$ Myr and $t \gtrsim 210$ Myr, respectively. The possibility of FRII-like lobe composition together with the presence of ‘warm spots’ in the radio lobes hint that the source could have been fed by an FRII-like jet for most of its lifetime, with the jet developing an FRI-like (dissipative) structure more recently (presumably due to a decrease in jet power).

We have presented the first detection of polarization at 150 MHz in NGC 6251, comprising a region of strong polarized emission in a knot in the northern jet and a weaker detection of polarization in the diffuse emission of the northern lobe. From these, taking advantage of the high Faraday resolution of LOFAR, we have placed upper limits on the strength of a magnetic field in the group environment with a single coherence scale $\Lambda_B$, with $B < 0.2(\Lambda_B/10\text{kpc})^{-0.5} \mu\text{G}$ for $\Lambda_B < 60$ kpc and $B < 13 \mu\text{G}$ for $\Lambda_B = 240$ kpc.

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