The quest for load-independent left ventricular chamber properties: Exploring the normalized pressure phase plane

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Abstract
The pressure phase plane (PPP), defined by dP(t)/dt versus P(t) coordinates has revealed novel physiologic relationships not readily obtainable from conventional, time domain analysis of left ventricular pressure (LVP). We extend the methodology by introducing the normalized pressure phase plane (nPPP), defined by 0 ≤ P ≤ 1 and −1 ≤ dP/dt ≤ +1. Normalization eliminates load-dependent effects facilitating comparison of conserved features of nPPP loops. Hence, insight into load-invariant systolic and diastolic chamber properties and their coupling to load can be obtained. To demonstrate utility, high-fidelity P(t) data from 14 subjects (4234 beats) was analyzed. PNR, the nPPP (dimensionless) pressure, where −dP/dtpeak occurs, was 0.61 and had limited variance (7%). The relative load independence of PNR was corroborated by comparison of PPP and nPPP features of normal sinus rhythm (NSR) and (ejecting and nonejecting) premature ventricular contraction (PVC) beats. PVCs had lower P(t)max and lower peak negative and positive dP(t)/dt values versus NSR beats. In the nPPP, +dP/dtpeak occurred at higher (dimensionless) P in PVC beats than in regular beats (0.44 in NSR vs. 0.48 in PVC). However, PNR for PVC versus NSR remained unaltered (PNR = 0.64; P > 0.05). Possible mechanistic explanation includes a (near) load-independent (constant) ratio of maximum cross-bridge uncoupling rate to instantaneous wall stress. Hence, nPPP analysis reveals LV properties obscured by load and by conventional temporal P(t) and dP(t)/dt analysis. nPPP identifies chamber properties deserving molecular and cellular physiologic explanation.

Introduction
The gold standard for characterization of chamber properties utilizes high-fidelity, micromanometric left ventricular (LV) pressures (P) as a function of time. The usual parameters include: maximum and minimum LV pressures (Pmax and Pmin), peak positive and peak negative rate of change of pressure (+dP/dtpeak and −dP/dtpeak), diastatic pressure, and end-diastolic pressure (EDP). For isovolumic relaxation (IVR) characterization, P from just after −dP/dtpeak to just before mitral valve opening is fit using a 2 or 3 parameter assumed exponential relationship (Weiss et al. 1976) which includes the time constant of isovolumic relaxation τ (Matsubara et al. 1995). LVP during the remaining >95% of the cardiac cycle is usually not analyzed.

Eucker et al. (2001) adopted the phase plane analysis method familiar in nonlinear dynamics (Strogatz 2008) to analyze LVP in the pressure phase plane (PPP) (Eucker et al. 2002). The oscillatory nature of P during the cardiac cycle generates closed PPP loops (analogs of limit cycles) allowing visualization of dP/dt versus P relation especially during the isovolumic phases when dP/dt reaches its respective systolic and diastolic maxima. PPP analysis has been used to characterize LV relaxation using various
mathematical assumptions (Leite-Moreira et al. 1999; Chung and Kovács 2007, 2008; Senzaki and Kass 2010). Senzaki and Kass (2010) fit the IVR segment in the PPP using a logistic model (parameter \( \tau_L \)) and showed that it provides a better fit to curved segments than the linear fit (\( \tau \)) provided by the exponential model. PPP analysis of IVR has also led to a predictive, causal kinematic model, where \( P(t) \) is the solution to the equation of motion of a damped oscillator (three parameters) allowing for fit of the model predicted solution from before \(-dP/dt_{peak}\) to MVO (Chung and Kovács 2008). PPP analysis provides a way to visualize spatiotemporal differences in LV hemodynamics (Ghosh and Kovács 2012) during IVR. It has also led to the development of a load independent index of IVR (Shmuylovich and Kovács 2008). Here, we extend PPP analysis and introduce the normalized pressure phase plane (\( nPPP \)) defined by \( -1 \leq dP/dt \leq 1, 0 \leq P \leq 1 \). Thus normalization eliminates load-dependent components of \( P \) and \( dP/dt \) and retains intrinsic contraction and relaxation features of the loops and helps to elucidate and characterize their differences and similarities.

Specifically, we focus on the values of normalized (dimensionless) pressure during isovolumic contraction (IVC) at \(+dP/dt_{peak} (P_{NC})\) and during IVR at \(-dP/dt_{peak} (P_{VR})\). Additionally, we analyze loops of normal sinus rhythm (NSR) and premature ventricular contraction (PVC) beats within and among subjects. In our exploration of the normalized pressure phase plane we hypothesize that \( nPPP \) analysis will elucidate novel chamber properties.

### Method

#### Derivation of normalized P and dP/dt contours

For each cardiac cycle, LVP was normalized according to:

\[
P_N(t) = \frac{(P(t) - P_{min})}{(P_{max} - P_{min})}
\]

which assures that \( P_{min} = 0 \) and \( P_{max} = 1 \). Figure 1A and B illustrate three beats before and after normalization.

The LV dP/dt was normalized according

\[
\left( \frac{dP}{dt} \right)_N = \frac{1}{2} \left( \frac{dP}{dt}_{max} + \frac{dP}{dt}_{min} \right)
\]

yielding \(-dP/dt_{peak} = -1\) and \(+dP/dt_{peak} = +1\) for each beat. Results are illustrated in Figure 1C and D with normalized loops in Figure 1E and F.

#### Inclusion criteria and data acquisition

We analyzed 17 datasets from our Cardiovascular Biophysics Laboratory database of simultaneous echocardiographic and high-fidelity hemodynamic recordings. Group clinical characteristics are listed in Table 1 (14 subjects) and Table 2 (three subjects). Prior to data acquisition, each subject provided signed, informed consent for

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**Figure 1.** Method for converting \( P \) and \( dP/dt \) into normalized contours and creating \( PPP \) and \( nPPP \) shown in two beats. \( P_C \) and \( P_R \) are marked in E and \( P_{NC} \) and \( P_{VR} \) are marked in F. See text for details.
our method of high-fidelity, multichannel micromano-
meter LV pressure and simultaneous echocardiography recor-
ding has been previously detailed (Chung and Kovács 2008; Shmylovich and Kovács 2008; Ghosh and Kovács 2012).
Briefly, simultaneous LV pressure and aortic root pressure
measurements were obtained using a 6-F triple transducer
pigtail-tipped pressure–volume conductance catheter
(SSD-1034; Millar Instruments, Houston, TX). The signal
was amplified and calibrated via standard transducer con-
trol units (TC-510; Millar Instruments). Catheter place-
ment was achieved by using fluoroscopy to cross the
aortic valve, noting that both (distal and mid) pressure
channels displayed LV pressure waveforms while the
proximal (3rd) sensor displayed aortic root pressures.
Pressure signals were input to clinical monitoring systems
(Quinton Diagnostics, Bothell, WA or GE Healthcare,
Milwaukee, WI) and a custom personal computer via a
research interface (Sigma-5DF; CD Leycom, Zoetermeer,
the Netherlands) at a sampling rate of 250 Hz. Conduc-
tance signals were stored but were not used in this study.
Ejection fraction was computed from the calibrated ven-
triculogram (33 mL of contrast at 11 mL/sec, via 6F pig-
tail catheter (Cordis Corporation, NJ) immediately after
hemodynamic recording.

### Hemodynamic data analysis

Pressure was converted for analysis via a custom Matlab
script (Matlab 6.0; MathWorks, Natick, MA). Data sets
were smoothed digitally by using a five-point average to
suppress noise in the derivative (Shmylovich and Kovác
2008; Ghosh and Kovács 2012), attenuating 50% of signal
at 40 Hz and 90% above 60 Hz, followed by calculation
of continuous dP/dt versus time t from the smoothed
data. For each beat, EDP and −dP/dtpeak were extracted
from PPP or equivalent time domain contours for both
pressure signals.

From the nPPP, the PNC and PNR were obtained as
shown in Figure 1 using a custom MATLAB script. For
all subjects, the mean value of $P_{\text{max}}$, $P_{\text{min}}$, $+dP/dt_{\text{peak}}$ and $-dP/dt_{\text{peak}}$ pressure at $+dP/dt_{\text{peak}} (P_c)$, pressure at $-dP/
dt_{\text{peak}} (P_R)$, $P_{\text{NC}}$ and $P_{\text{NR}}$ were calculated and saved.

We selected three subjects’ datasets for PVC analysis.
PVCs were first identified from ECG recordings and then
classified as ejecting PVCs (E-PVC) or nonejecting PVCs
(NE-PVC) by comparing LVP to the simultaneous aortic
root pressure. If the LV pressure and the aortic root pres-
sure recordings intersected and the aortic pressure showed
a rise and fall concordant with the LV pressure it was
classified as E-PVC otherwise it was classified as NE-PVC
as shown in Fig 2. For the subjects the mean value of
$P_{\text{max}}$, $P_{\text{min}}$, $+dP/dt_{\text{peak}}, -dP/dt_{\text{peak}}$, $P_c$, and $P_R$ were calcu-
lated for NSR beats as well as E-PVC beats and NE-PVC
beats. Mean values for $P_{\text{NC}}$ and $P_{\text{NR}}$ in NSR, E-PVC and
NE-PVC beats were calculated.

### Table 1. Subject demographics (n = 14).

| Parameter        | Mean ± SD |
|------------------|-----------|
| Age (years)      | 62 ± 9    |
| Gender           | 7M/7F     |
| Height (cm)      | 167 ± 9   |
| Weight (lb)      | 182 ± 43  |
| BMI (kg/m²)      | 29.7 ± 7.8 |
| EDP (mm Hg)      | 18 ± 3    |
| ESP (mm Hg)      | 105 ± 7   |
| Ejection fraction (%) | 72 ± 8    |
| No. of beats     | 302 ± 43  |
| Hypertension     | 7 (50%)   |

Values are mean ± standard deviation or number (% of total subjects).

### Table 2. Subject demographics for intrasubject (n = 3) PVC analysis.

| Subject | A1 | A2 | A3 |
|---------|----|----|----|
| Age     | 43 | 63 | 56 |
| Gender  | M  | M  | M  |
| Ejection fraction (%) | 81 | 24 | 54 |
| Height (cm) | 196 | 183 | 170 |
| Weight (lb) | 335 | 206 | 165 |
| BMI (kg/m²) | 40  | 28  | 26  |
| EDP (mm Hg) | 17  | 15  | 10  |
| Hypertension | +  | +   | –   |
| CAD/previous MI | –  | +   | –   |
| Total NSR beats | 150 | 232 | 210 |
| Total PVC beats | 9 (NE) | 78 (E) | 17 (E) |

+/− denote presence or absence of condition. NE, nonejecting PVC; E, ejecting PVC.
Statistical analysis

The mean, standard deviation (SD), maximum and minimum values were calculated for the points of interest in the regular PPP and nPPP. In addition, to determine variation we calculated the coefficient of variation, defined as the ratio of standard deviation to the mean value of the parameter, (as shown in Table 3) expressed as a percentage for the 14 subjects included in the intersubject analysis. To compare NSR and PVC features we used the Student’s two-tailed t-test to determine statistical significance, with \( P < 0.05 \) denoting significance.

Results

Table 1 shows the subject characteristics for the 14 subjects. Table 3 provides the mean, SD, minimum, maximum, and the coefficient of variation values of the points of interest in the regular PPP and nPPP based on 4234 cardiac cycles. By definition, normalization reduced the variation in \( P_{\max}, P_{\min}, +dP/dt_{\text{peak}} \), and \( -dP/dt_{\text{peak}} \) to 0. The variation of \( P_C \) (9.6%) changed slightly compared with \( P_{\text{NC}} \) (10.5%) while the variation \( P_{\text{NR}} \) (6.6%) decreased compared with \( P_R \) (11.3%). The variation of both nEDP (27.1%) and nESP (8.9%) increased in comparison to EDP (17.9%) and ESP (6.9%). Among all these \( P_{\text{NR}} \) had the lowest variation. To illustrate intersubject variation in PPP loop shape and features Figure 3A shows individual, superimposed beats from three subjects. Figure 3B shows same beats in the nPPP, illustrating the effect of normalization in eliminating the differences in Figure 3A.

To investigate nPPP features and determine the effect of normalization on \( P_{\text{NR}} \), we compared NSR beats to E-PVCs and NE-PVCs in the same subject. We selected three datasets that had significant number of PVCs to permit statistical analysis. Table 2 shows the clinical characteristics. Figure 4 shows PPP and nPPP for a NSR and E-PVC beat in the same subject. For clarity, Figure 4C and D magnifies the \( P_{\text{NC}} \) and \( P_{\text{NR}} \) portions of Figure 4B. As these figures illustrate, normalization aids in visualizing features masked by the differences in \( P_{\max}, P_{\min}, +dP/dt_{\text{peak}} \), and \( -dP/dt_{\text{peak}} \).

In Subject B1 (see Table 2) we compared NE-PVCs to NSR beats. In concordance with previous results (Carroll et al. 1983), we found that \( P_{\max}, +dP/dt_{\text{peak}} \), and \( -dP/dt_{\text{peak}} \) were significantly lower in magnitude in the PVC beats \((P < 0.01)\). While \( P_R \) was statistically different between the two types of beats \((P < 0.001)\); \( P_{\text{NR}} \) was not statistically different \((P = 0.09)\). In subjects B2 and B3 (Table 2), we compared NSR beats to E-PVC beats but not to NE-PVCs because of limited numbers. Similar to subject B1, we found that in B2 and B3, \( P_{\max}, +dP/dt_{\text{peak}}, \) and \( -dP/dt_{\text{peak}} \) were much lower in magnitude in the PVC beats \((P < 0.0001)\). Also \( P_R \) was statistically different between the two types of beats; the value of \( P_{\text{NR}} \) was not statistically

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**Table 3.** Group values \((n = 14)\) of hemodynamic parameters.

| Parameter          | Mean   | SD   | Min   | Max   | Variation |
|--------------------|--------|------|-------|-------|-----------|
| \( P_{\max} \) (mm Hg) | 137    | 17   | 119   | 165   | 12.1%     |
| \( P_{\min} \) (mm Hg) | 9.3    | 3    | 3.6   | 13.4  | 29.7%     |
| \( dP/dt_{\max} \) (mm Hg/sec) | 1257   | 136  | 1062  | 1531  | 10.8%     |
| \( dP/dt_{\min} \) (mm Hg/sec) | -1496  | 182  | -1834 | -1266 | 12.2%     |
| \( P_C \) (mm Hg)    | 61     | 6    | 49    | 72    | 9.6%      |
| \( P_R \) (mm Hg)    | 87     | 10   | 75    | 104   | 11.3%     |
| \( P_{\text{NC}} \) (dimensionless) | 0.41   | 0.04 | 0.34  | 0.48  | 10.5%     |
| \( P_{\text{NR}} \) (dimensionless) | 0.61   | 0.04 | 0.56  | 0.69  | 6.6%      |
| EDP (mm Hg)         | 18     | 3    | 13    | 23    | 17.9%     |
| ESP (mm Hg)         | 105    | 7    | 93    | 116   | 6.9%      |
| nEDP (dimensionless) | 0.07   | 0.02 | 0.03  | 0.1   | 27.1%     |
| nESP (dimensionless) | 0.76   | 0.07 | 0.64  | 0.9   | 8.9%      |

Coefficient of variation is defined in Methods. SD, Standard deviation.
different \( (P = 0.09 \text{ and } P = 1) \). This suggests that \( P_{NR} \) remains essentially unaltered between NSR and PVC beats. The mean value of \( P_{NR} \) (0.64) in the three datasets with PVCs was comparable to the value of \( P_{NR} \) (0.61) obtained from the first part of the study analyzing 14 datasets. While PC did not differ between NSR and PVC due to large intra-subject variation (12.3%), \( P_{NC} \) did not differ in spite of the low beat to beat variation (6.3%) indicating a much smaller distribution of \( P_{NR} \) values in NSR and PVC beats. The mean values of the hemodynamic parameters of the \( \text{PPP} \) and the \( n\text{PPP} \) in NSR and PVC beats are given in Table 4 along with measures of statistical significance.

### Discussion

Normalization of diastolic physiologic data has been employed in a different context previously. Klotz et al. (2006) proposed a method to estimate the end-diastolic pressure–volume relationships by normalizing LV volumes. They found that normalization generated end-diastolic pressure–volume curves having the same shape across different species and pathologies.

The phase plane method has been used in biological and physiological systems (Paniflov and Hogeweg 1995; Keener and Sneyd 1998). LV pressure phase plane analysis, a component of 4-dimensional physiologic hyperspace (Eucker et al. 2002), has been previously employed (Eucker et al. 2001; Chung et al. 2006; Chung and Kovács 2007) to identify new cardiac cycle features. In the quest to identify load-independent chamber properties we explored LV hemodynamics in the \( n\text{PPP} \). Normalization maps the variable maximum and minimum pressure and \( dP/dt \) limits of consecutive beats to the same values and thereby removes loading effects while contraction and relaxation related loop shape features are retained. We evaluated IVC and IVR loop features in different

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**Table 4. Mean hemodynamic parameters in NSR versus PVC analysis subjects.**

| Parameter | Subject B1 | Subject B2 | Subject B3 |
|-----------|------------|------------|------------|
|           | NSR       | PVC        | NSR       | PVC        | NSR       | PVC        |
| \( P_{max} \) (mm Hg) | 116       | 101\(^2\) | 140       | 127\(^2\) | 132       | 92\(^2\)   |
| \( P_{min} \) (mm Hg) | 11        | 11         | 12        | 12         | 9         | 8          |
| \( dP/dt_{max} \) (mm Hg/sec) | 996       | 758\(^2\) | 1190      | 1026\(^2\) | 1007      | 652\(^2\)  |
| \( dP/dt_{min} \) (mm Hg/sec) | -1121     | -861\(^1\) | -1169     | -1019\(^2\) | -1136     | -584\(^2\) |
| \( P_{C} \) (mm Hg) | 61        | 52         | 73        | 73         | 53        | 47         |
| \( P_{A} \) (mm Hg) | 73        | 61\(^2\)   | 99        | 88\(^2\)   | 87        | 60\(^2\)   |
| \( P_{NC} \) | 0.47      | 0.45       | 0.48      | 0.53\(^2\) | 0.36      | 0.46\(^1\) |
| \( P_{NR} \) | 0.63      | 0.59       | 0.67      | 0.66       | 0.63      | 0.63       |
| \( EDP \) (mm Hg) | 16        | -NA-       | 16        | -NA-       | 16        | -NA-       |
| \( ESP \) (mm Hg) | 106       | -NA-       | 123       | -NA-       | 89        | -NA-       |

The number of beats is given in Table 2.

\(^1P < 0.01.\)

\(^2P < 0.0001.\)
subjects to characterize differences and similarities. We also compared NSR beats to PVCs in three subjects. Both studies showed that \( P_{NR} \) remains essentially invariant while other \( nPPP \) points of interest varied significantly. Hence, \( nPPP \) analysis indicates that \( P_{NR} \) is closely conserved.

### Load dependence of LV relaxation

Chamber relaxation is known to be determined in part by cross-bridge uncoupling and other load-dependent mechanisms (Katz 1930; Karliner et al. 1977; Brutsaert et al. 1980; Gaasch et al. 1980; Hori et al. 1985; Eichhorn et al. 1992; Chemla et al. 2000; Janssen 2010; Senzaki and Kass 2010). Cross-bridge uncoupling requires dissociation of \( Ca^{2+} \) from troponin and its sequestration in the sarcoplasmic reticulum (Bers 2000; Rice and de Tombe 2004). Increased afterload, quantified by end-systolic pressure or volume has a slowing effect on the rate of pressure decay during IVR (Chemla et al. 2000). Other studies have reported that in normal hearts IVR is load independent while failing hearts show increased load sensitivity (Starling et al. 1987; Little 1992; Prabhu 1999). In failing hearts, \(-\frac{dP}{dt}_{peak}\) is lower than in normal hearts (Prabhu 1999) and its cause remains uncertain.

#### Table 5. List of Abbreviations and units of measurement.

| Abbreviation | Full Term                        | Unit            |
|--------------|----------------------------------|-----------------|
| PPP          | Pressure phase plane             | -NA-            |
| P            | Left ventricular pressure        | mm Hg           |
| \( \frac{dP}{dt} \) | Time rate of change of LV pressure | mm Hg/\text{sec} |
| \( P_{min} \) | Minimum LV pressure             | mm Hg           |
| \( P_{max} \) | Maximum LV pressure             | mm Hg           |
| \( +\frac{dP}{dt}_{peak} \) | Peak positive \( \frac{dP}{dt} \) | mm Hg/\text{sec} |
| \( -\frac{dP}{dt}_{peak} \) | Peak negative \( \frac{dP}{dt} \) | mm Hg/\text{sec} |
| \( P_C \)    | Pressure at \( +\frac{dP}{dt}_{peak} \) | mm Hg           |
| \( P_R \)    | Pressure at \( -\frac{dP}{dt}_{peak} \) | mm Hg           |
| EDP          | End-diastolic pressure           | mm Hg           |
| ESP          | End-systolic pressure            | mm Hg           |
| \( nPPP \)  | Normalized pressure phase plane  | -NA-            |
| \( P_{NC} \) | Normalized pressure at \( +\frac{dP}{dt}_{peak} \) | Dimensionless |
| \( P_{NR} \) | Normalized pressure at \( -\frac{dP}{dt}_{peak} \) | Dimensionless |
| nEDP         | Normalized end-diastolic pressure | Dimensionless   |
| nESP         | Normalized end-systolic pressure | Dimensionless   |
| NSR          | Normal Sinus Rhythm             | -NA-            |
| E-PVC        | Ejecting premature ventricular contraction | -NA-          |
| NE-PVC       | Nonejecting premature ventricular contraction | -NA-         |
| IVR          | Isovolumic relaxation           | -NA-            |
| IVC          | Isovolumic contraction          | -NA-            |

#### Figure 4.

(A) PPP from two beats – NSR and E-PVC recorded from Subject B3. (B) Normalization of the same two beats. (C) Magnified view of \( nPPP \) top portion, including \( +\frac{dP}{dt}_{peak} \). (D) Magnified view of \( nPPP \) bottom portion including \( -\frac{dP}{dt}_{peak} \). Data points were smoothed using three point moving average. See text for details.
Intersubject comparison of \( nPPP \)

To determine if \( nPPP \) can characterize chamber properties that are minimally load dependent or are load independent, we analyzed data from 14 subjects (302 beats/subject, 4234 beats total; Table 1). Normalization eliminated the intersubject variance of \( P_{\text{max}}, P_{\text{min}}, +dP/dt_{\text{peak}}, \) and \( -dP/dt_{\text{peak}} \). Normalization did not alter the variation of pressure at which \( +dP/dt_{\text{peak}} \) occurs (\( P_C \) variance = 10% vs. \( P_{\text{NC}} \) variance = 11%), but it did decrease the variation of pressure at which \( -dP/dt_{\text{peak}} \) occurs (Table 3) (\( P_R \) variance = 11%, vs. \( P_{\text{NR}} \) variance = 6.6%). Thus, in contrast to IVC, normalization generated a much smaller variation in \( P_{\text{NR}} \) during IVR in PVCs suggesting a (relatively) conserved intrinsic relaxation mechanism.

Hemodynamics of premature ventricular contractions

PVCs provide natural (in contrast to pharmacologic) beat-to-beat load variation. Many studies have utilized PVCs to characterize load effects in contraction and relaxation. Carroll et al. (1983) studied IVR during PVCs and found that PVCs enhance shortening and augment restoring forces producing a smaller end-systolic chamber. PVCs also delay inactivation and prolong relaxation, generating increased values of \( \tau \) while impairing LV filling (Stoddard et al. 1989). PVCs have also been employed to more extensively validate a load independent index of diastolic function (Boskovski et al. 2008).

Effect of normalization on PVC hemodynamics

We exploited PVC generated load variation to assess load-dependent features in the \( PPP \) and the \( nPPP \). Information on the PVC datasets is given in Table 2 and Table 4. Figure 4A shows a NSR and E-PVC beat in the \( PPP \) and Figure 4B shows the same beats in \( nPPP \). As seen in the figure, E-PVC has lower values of \( P_{\text{max}}, +dP/dt_{\text{peak}} \) and \( -dP/dt_{\text{peak}} \). \( P_C \) was not significantly different between NSR and PVC beats although large beat-to-beat variation in each subject was present. \( P_R \) was significantly lower in PVCs in all the three subjects (\( P < 0.001 \)).

The value of \( P_{\text{NR}} \) was not significantly different among the three subjects between NSR and PVC beats. This revealed that there is essentially no change in the dimensionless pressure at which the peak rate of pressure decay occurred in both NSR and PVC beats. This value is comparable to the value of \( P_{\text{NR}} \) obtained from the first part of the study (Table 3, \( P_{\text{NR}} \) = 0.61). \( P_{\text{NC}} \) on the other hand was higher in E-PVC compared with NSR. Hence unlike contraction, which shows changes in the rate of pressure rise as a function of pressure in PVCs, the rate of pressure decay as a function of pressure is essentially unchanged during IVR in PVCs suggesting a (relatively) conserved intrinsic relaxation mechanism.

Physiological significance of normalization and possible mechanism

LV contraction and relaxation involves actin–myosin cross-bridge coupling and uncoupling regulated by Ca\(^{2+}\) bound to troponin (Baker et al. 1998; Bombardini 2005; de Tombe et al. 2010) and further modulated by the loading conditions involving pressure and its variation. Studies have attempted to understand the contribution of load as factors in contraction and relaxation (Brutsaert et al. 1980; Hori et al. 1985; Starling et al. 1987; Little 1992; Prabhu 1999) by physiologic, pharmacologic, or surgical interventions to modify load and evaluate response.

Some of the factors determining these intrinsic mechanisms include calcium cycling, sarcomere kinetics, mitochondrial (ATP) function, extracellular matrix, etc. The similar variation of \( P_C \) and \( P_{\text{NC}} \) (Table 3) suggests that its variation is determined by factors other than load. On the other hand, the reduced variation of \( P_{\text{NR}} \) as compared to \( P_R \) suggests that its variation is load dependent but the intrinsic mechanism that constrains \( P_{\text{NR}} \) to be in the 0.61–0.64 range is conserved. This underscores that \( nPPP \) is not merely a scaled down version of the regular \( PPP \). Rather normalization removes \( P \) and \( dP/dt \) magnitude effects while maintaining shape-based features.

Maintenance of shape-based features was borne out by the intersubject PVC analysis. The value of \( P_{\text{NR}} \) was similar in NSR and PVC beats within and across subjects (Table 4). Its value was also similar to the value reported in the intersubject analysis (Table 3). This permits the inference that intrinsic relaxation mechanisms are more...
(tightly regulated) conserved than intrinsic contraction mechanisms. Moreover, contractility and the associated value of P_{NC} in NSR and E-PVC beats is governed by the beat-to-beat variation of preload and afterload while in NE-PVCs it is primarily determined by the Frank–Starling Law and the timing of the PVC relative to the prior beat. Hence, an nPPP based prediction is that because of the beat-to-beat variation of load, we expect P_{NC} to have larger variation than P_{NR}. Our observations corroborate this prediction. Sarcomere kinetics is a major determinant of relaxation mechanisms (Piroddi et al. 2007; Stehle et al. 2009). Two features of sarcomere kinetics likely to have a bearing on the limited variation of P_{NR} include (Little et al. 2012) – (1) kinetics of Ca^{2+} binding and dissociation from troponin and (2) cross-bridge attachment/detachment and subsequent sarcomere shortening/lengthening. The relative constancy of P_{NR} suggests that the ratio of maximum rate of cross-bridge dissociation to instantaneous pressure (force, wall stress) at which that maximum dissociation rate takes place is tightly constrained. This preliminary, proof of concept study demonstrates the utility of PPP normalization in elucidating novel LV diastolic properties.

**Limitations**

The main limitations pertain to data acquisition. As noted previously (Ghosh and Kovács 2012), calibration, catheter placement, and orientation with respect to the LV axis may have a slight effect on pressure recordings. However, calibration offsets the pressure by a constant value which should not affect the normalization process. Calibration and drift are mitigated by pre- and postcalibration of transducers to zero hydrostatic pressure in a 37°C saline bath. Other issues involving signal processing have been addressed previously (Chung and Kovács 2008; Shmuylovich and Kovács 2008; Ghosh and Kovács 2012). Noisy beats were not analyzed. Moreover, the large (average) number of beats studied in every subject (302) mitigates the effect of noise to an acceptable degree.

As this is a proof of concept study, the number of datasets analyzed is necessarily limited although the 4234 cardiac cycles analyzed mitigates that limitation to an acceptable degree. Although eight of the datasets analyzed in this study have been previously analyzed for different purposes (16), repeat analysis using a different method (normalization) to test a different hypothesis (load independence of phase plane loop features) is appropriate. Relative physiologic uniformity is achieved as a result of enrollment criteria (normal ejec tion fraction, no coronary artery disease or myocardial infarctions, no diabetes). P and dP/dt values were not very different (<50% variation in P_{max} +dP/dt_{peak}, P_C, and P_R values). This limitation is mitigated by the second part of the study where we compared NSR to PVC beats in the same subject. The PPP in PVC is much smaller and has a different shape from a NSR PPP (Fig. 3; Chung and Kovács 2008). In spite of this, P_{NSR} remained an essentially conserved feature among the three subjects. However, we only studied PVCs in three subjects, which is insufficient to draw definitive conclusions regarding trends. Hence, additional studies are needed to elucidate the magnitude of these changes and differentiate between the changes in E-PVCs versus NE-PVCs. Further work in the PPP and physiologic hyperspace is needed involving a greater sample size and specific pathophysiologic states.

**Conclusions**

We introduce the nPPP for LV hemodynamic analysis. Normalization removes beat-to-beat and intersubject variation in P and dP/dt limits and thereby, minimizes load effects. We tested applicability in ~4400 beats in 14 subjects. In the nPPP, the variation of P_{NR}, the (dimensionless) pressure at which –dP/dt_{peak} was inscribed, was very substantially reduced. Comparison of NSR beats to both ejecting and nonejecting beats PVCs revealed that P_{NSR} remained tightly controlled. The observed near constancy of P_{NR} reveals a new aspect of the physiology of diastole and indicates the existence of intrinsic (intracellular) IVR mechanisms for which a possible mechanism is discussed. Thus, nPPP analysis elucidates novel LV chamber properties, and identifies potential research targets in need of molecular and cellular physiologic explanation.

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**Conflict of Interest**

None declared.

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