Abstract. Convection plays an essential role in the emerging intensity for many stars that will be observed by Gaia. Convective-related surface structures affect the shape, shift, and asymmetry of absorption lines, the photocentric and photometric variability causing bias in Gaia measurements. Regarding the importance of Gaia mission and its goals, it is mandatory to have the best models of the observed stars. 3-D time-dependent hydrodynamical simulations of surface convection are crucial to model the photosphere of late type stars in a very realistic way. These simulations are an important tool to correct the radial velocities and to better estimate the parallaxes and photometric variability.

1. Introduction
The main goal of the Gaia mission [1, 2] is to determine high-precision photocentric parameters (i.e., positions, parallaxes, and proper motions) for one billion objects with apparent magnitudes in the range $5.6 \leq V \leq 20$ and kinematic velocities of about 100 millions of stars with a precision of $\sim 1 \text{ km s}^{-1}$ up to $V \leq 13$. These data along with multi-band and multi-epoch photometric data will allow to reconstruct the formation history, structure, and evolution of the Galaxy. Convection plays a crucial role in the formation of spectral lines and deeply influences the shape, shift, and asymmetries of lines in late type stars which will represent most of the objects that will be observed by Gaia. In addition to this, granulation-related variability that is considered as "noise" must be quantified in order to better characterize any resulting systematic error on the parallax and photometric determinations.

Realistic modelling of stellar atmospheres is therefore crucial for a better interpretation of future Gaia data and, in this context, three-dimensional radiative-hydrodynamical models are needed for a quantitative correction of the radial velocities (few hundreds km s$^{-1}$) for all the stars observed and, in evolved stars, for the determination of the photocenter positions.
2. Surface convection simulations and radiative transfer calculations
We adopted here time-dependent, three-dimensional (3-D), radiative-hydrodynamical (RHD) surface convection simulations of different stars across the Hertzsprung-Russell diagram (Table 1). The simulations have been carried out using:

- The box-in-a-star setup with Stagger-Code\(^1\). These models cover only a small section of the surface layers atop the deep convection zone, and the numerical box includes a number of convective cells proportional to the surface gravity. They have constant gravity, the lateral boundaries are periodic, and the radiation transport module relies on a Feautrier scheme applied to long characteristics.

- The star-in-a-box setup with CO\(^5\)BOLD code [3, 4, 5]. These simulations cover the whole convective envelope of the star and have been used to model red supergiant (RSG) stars [3, 5] and Asymptotic Giant Branch stars [4] so far. The computational domain is an equidistant cubic grid in all directions, and the same open boundary condition is employed for all sides of the computational box.

The transition between the box-in-a-star and star-in-a-box occurs around \(\log g \sim 1\), when the influence of sphericity and the ratio between granule size versus stellar diameter become important; the star-in-a-box global models are then needed, but they are highly computer-time demanding and difficult to run so that there are only very few models available so far.

We used the 3-D pure-LTE radiative transfer code Optim3D [6] to compute spectra and intensity maps from the snapshots of the RHD simulations listed in Table 1. The code takes into account the Doppler shifts due to convective motions. The radiative transfer equation is solved monochromatically using extinction coefficients pre-tabulated with the same chemical compositions as the RHD simulations and using the same extensive atomic and molecular opacity data as the latest generation of MARCS models [7]. We assumed a zero micro-turbulence since the velocity fields inherent in 3-D models are expected to self-consistently and adequately account for non-thermal Doppler broadening of spectral lines.

3. Kinematic radial velocities and correction of convective shifts
A convenient and usual way to estimate the kinematic radial velocity of a star is commonly made from a measurement of its spectroscopic radial velocity. Gaia is provided with a dedicated radial velocity spectrometer (RVS, [11]) with a resolving power of (at best) 11,500 centered on the Ca II triplet in the spectral band from 8480 Å to 8750 Å. It is well known that photospheric absorption lines in many stars are blueshifted as a result of convective movements in the stellar atmosphere. In fact, hot, bright, and rising (i.e., blueshifted) convective elements contribute more photons than cool dark shrinking gas, and as a consequence, the absorption lines appear blueshifted [12, 13]. This effect is one of the systematic errors of spectroscopic measurements with RVS [14, 15] and will be taken into account by the Gaia analysis pipeline using 3-D RHD simulations [16] which account for turbulent movements and therefore do not require the traditional micro- and macro-turbulence velocities used in hydrostatic models.

We computed synthetic spectra in RVS domain using Optim3D for all the models reported in Table 1. The spectra were computed along rays of four \(\mu\)-angles \([0.88, 0.65, 0.55, 0.34]\) and four \(\phi\)-angles \([0^\circ, 90^\circ, 180^\circ, 270^\circ]\), after which we performed a disk integration and a temporal average over all selected snapshots. It is important that the total time covered by the simulations is such that there are no trends in the lineshift if a subset of snapshots is used for the calculations. This has been verified by [17] for the simulation with \(T_{\text{eff}}=4630\) K and \(\log g=1.6\)

\(^1\) www.astro.ku.dk/~aake/papers/95.ps.gz
Table 1. 3-D hydrodynamical model atmospheres used in this work. The symbols refer to Figs. 5, 6, 7, and 8.

| Stellar type | $T_{\text{eff}}$ [K] | log $g$ | [Fe/H] | Mass [$M_\odot$] | Ref. | Symbol |
|--------------|---------------------|--------|--------|-----------------|------|--------|
| K giant      | 4700                | 2.2    | 0.0    | ...             |      |        |
| K giant      | 4720                | 2.2    | -1.0   | ...             |      |        |
| K giant      | 5035                | 2.2    | -0.8   | ...             |      |        |
| K giant      | 5130                | 2.2    | -3.0   | ...             |      |        |
| K giant      | 4630                | 1.6    | -3.0   | ...             |      |        |
| F star       | 6500                | 4.0    | 0.0    | ...             |      |        |

Local simulations with Stagger-Code

| Stellar type | $T_{\text{eff}}$ [K] | log $g$ | [Fe/H] | Mass [$M_\odot$] | Ref. | Symbol |
|--------------|---------------------|--------|--------|-----------------|------|--------|
| K giant      | 4700                | 2.2    | 0.0    | ...             |      |        |
| K giant      | 4720                | 2.2    | -1.0   | ...             |      |        |
| K giant      | 5035                | 2.2    | -0.8   | ...             |      |        |
| K giant      | 5130                | 2.2    | -3.0   | ...             |      |        |
| K giant      | 4630                | 1.6    | -3.0   | ...             |      |        |
| F star       | 6500                | 4.0    | 0.0    | ...             |      |        |

Global simulations with CO$_5$BOLD

| Stellar type | $T_{\text{eff}}$ [K] | log $g$ | [Fe/H] | Mass [$M_\odot$] | Ref. | Symbol |
|--------------|---------------------|--------|--------|-----------------|------|--------|
| K giant      | 4700                | 2.2    | 0.0    | ...             |      |        |
| K giant      | 4720                | 2.2    | -1.0   | ...             |      |        |
| K giant      | 5035                | 2.2    | -0.8   | ...             |      |        |
| K giant      | 5130                | 2.2    | -3.0   | ...             |      |        |
| K giant      | 4630                | 1.6    | -3.0   | ...             |      |        |
| F star       | 6500                | 4.0    | 0.0    | ...             |      |        |

Figure 1. Spectra in the Gaia-RVS domain for the local simulations of Table 1. An offset has been added to the colored curves.

Figure 2. Enlargements of Fig. 1 around a Ca II line.

in Table 1. Ramirez et al. [17] found that the sequence was sufficiently long to ensure that the results are statistically significant and the comparison with observations is also very good. However, for the other K giant models we have not yet done any comparisons with observations. Figures 1 and 2 show the results for the local simulations, and Fig. 3 and 4 for the global ones. It is noticeable how the Ca II triplet ($\lambda$ =8498.02, 8542.09, 8662.14 Å) is well visible in all the stars, even at low metallicity.

Following the work of [18], we determined the position, the depth and the width of Ca II triplet and of 20 Fe I lines selected to be non-blended lines and to cover the spectral domain of the RVS [19]. For this preliminary work, we fitted the absorption lines with a Gaussian function. Figure 5 shows that Fe I lines are mostly blueshifted (except for few cases with low-excitation
potentials). The convective lineshift (Table 1, $\Delta \lambda_{\text{FeI}}$) appears stronger for high-excitation lines and ranges, on average, from $-0.22$ km s$^{-1}$ (K giant with $[\text{Fe/H}] = -3.0$) to $-0.75$ km s$^{-1}$ (F star). The amplitude of the shift increases from K-type giants to the F-type star as a consequence of the more vigorous convective movements. Moreover, the Ca II triplet lines are redshifted because these lines are formed in the upper part of the photosphere where the granulation pattern is reversed. The lineshift is particularly strong in the case of the F-type star (Table 1, $\Delta \lambda_{\text{CaII}}$).

![Figure 3](image1.png) ![Figure 4](image2.png)

**Figure 3.** Spectra in the Gaia-RVS domain for the global simulations of Table 1. **Figure 4.** Enlargements of Fig. 3 around a Ca II line.

The lineshifts are not the same for all the lines in the RVS spectra. The precise amount of shift depends on the strength of the absorption line (and hence on the stellar metallicity), since different lines are formed at different atmospheric depths and thus experience different granulation contrasts and convective velocities. In fact, Fig. 7 shows that there is a correlation between lineshifts and line depth indicating that weaker lines (with high excitation potential) are in general more shifted than deep lines (low excitation potential). This picture is also supported by Fig. 5. In addition to this, Fig. 8 shows that there is no apparent connection with the line

![Figure 5](image3.png) ![Figure 6](image4.png)

**Figure 5.** Convective shifts of 20 Fe I from [19] as a function of excitation potentials for local simulations of Table 1. For metal-poor stars, only visible lines in the spectra are reported. **Figure 6.** Convective shifts of 20 Fe I from [19] as a function of excitation potentials for global simulations of Table 1.
RSGs show a completely different behavior (Fig. 6) with strong redshifted Fe I up to 2.80 km s\(^{-1}\) and blueshifted Ca II up to 8 km s\(^{-1}\) (Table 1). The reason is likely connected with the reversed-C shape of line bisectors observed by [21] in the prototypical RSG Betelgeuse and caused by a peculiar and vigorous convection, but further investigations are needed and still in progress with RHD simulations.

In conclusion, velocity shifts of F- and K-giant stars are of the order of RVS accuracy (~1 km s\(^{-1}\)), and they are even larger for RSG stars.

4. Photometric and photocentric variabilities and impact on parallaxes

Massive evolved stars such as RSG stars give rise to large granules comparable to the stellar radius in the \(H\) and \(K\) bands, and an irregular pattern in the optical region [22]. These surface inhomogeneities vary with time and may strongly affect the photometric and astrometric measurements of Gaia.

Figure 9 displays the variability of a RSG during a period comparable with the Gaia mission in the blue and red photometric bands of Gaia. The photometric system of Gaia will be used to characterize the stellar effective temperature, surface gravity and metallicity [23]. The simulations show fluctuations of up to \(0.28\) in the blue and up to \(0.15\) in the red bands over 5 years. The photometric fluctuations of RGSs are not negligible and the uncertainties in [Fe/H], \(T_{\text{eff}}\) and log \(g\) for these stars with \(G < 15\) should be revised upwards due to their convective movements [24].

The simulated surface of RSGs (Fig. 10) displays high-contrast structures with spots up to 50 times brighter than the dark ones with strong changes over some weeks. This aspect is connected with the underlying granulation pattern, but also with dynamical effects such as shocks and waves which dominate at optical depths smaller than 1 [22]. The convective-related surface structures in the Gaia \(G\) band strongly affect the position of the photocenter and cause temporal fluctuations (left-hand panel of Fig. 11). The photocenter excursion is large, since it goes from 0.005 AU to 0.3 AU over 5 years of simulation and it is on average 0.132 AU (i.e., \(\sim 3\%\) of the stellar radius). This value corresponds to a photocenter excursion of \(\sim 10\) \(\mu\)as for...
Figure 9. Spectral fluctuations in the blue (left-hand panel) and red (right-hand panel) Gaia photometric band [25] for a RSG simulation. The black curve is the average flux over ~5 years covered by the simulation, while the shades areas mark the range of maximum and minimum fluctuations. The spectra have been smoothed to the Gaia photometric resolution of $R \sim 50$ [23]. Figures are adopted from [24].

a star at 1 kpc, which is comparable to the Gaia accuracy of ~10 μas for stars brighter than $G=10$.

Chiavassa et al. [24] calculated the Gaia parallax using the Gaia Object Generator v7.0, GOG2 [26] for RSGs with surface brightness asymmetries from RHD simulations ($\varpi_{\text{spot}}$) and without ($\varpi$). Figure 11 (right-hand panel) shows that there is a systematic error of a few percent. The systematic error may be up to 15 times the formal error $\sigma_{\varpi}$ [24]. Although this errorbar should be used to revise $\sigma_{\varpi}$, there is little hope for correcting the Gaia parallaxes of RSGs for this parallax error without knowing the run of the photocentric shift of each star under consideration. Thus, it might be of interest to monitor the photocentric deviations of a number of selected RSGs during the Gaia mission using interferometry and/or spectroscopy to obtain valuable information about the photocentric position and to correct the resulting parallaxes using RHD predictions.

5. Conclusions and perspectives

3-D hydrodynamical simulations of surface convection are a very important tool to account for convective shift corrections on the kinematic radial velocities, parallaxes and photometry.

With the increase of compute power, it is currently possible to compute 3-D model grids rather easily on reasonable timescales. In this framework, the 3-D local model grid computed with STAGGER-CODE (see the contribution of R. Collet in this Volume) will soon be available, together with the synthetic spectra in RVS domain (before Gaia launch date, mid 2013). The grid will include about 130 models with $T_{\text{eff}}$ ranging from 4000 K to 6500 K, $\log g$ from 1.5 to 5 and [Fe/H]=0.0, −1.0, −2.0, −3.0. These models will not be sufficient to represent all the stars observed by Gaia and thus, following [16], we plan to apply 3-D convective corrections to spectroscopic radial velocities obtained with less sophisticated models and templates.

2 http://gaia-gog.cnrs.fr
Figure 10. Synthetic map of intensity (the range is \([0 - 230000] \text{ erg s}^{-1} \text{ cm}^{-2} \text{ Å}^{-1}\)) in the Gaia G band [25]. Figure adopted from [24].

Figure 11. Left-hand panel: photocenter displacement as a function of time for a RSG simulation. Each point is a snapshot 23 days apart for a total of 5 years of simulation (comparable to the duration of the Gaia mission). Right-hand panel: relative difference between the parallaxes computed with and without the photocentric motion of the left-hand panel, as a function of the distance. Figures adopted from [24].

Acknowledgments
The authors thank the Rechenzentrum Garching (RZG) for providing the computational resources necessary for this work. A.C. is supported in part by an Action de recherche concertée (ARC) grant from the Direction générale de l’Enseignement non obligatoire et de la Recherche scientifique - Direction de la Recherche scientifique - Communauté française de Belgique. A.C. is supported by the F.R.S.-FNRS FRFC grant 2.4513.11.

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