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DOI
10.3390/polym10080845

Publication date
2018

Document Version
Final published version

Published in
Polymers

Citation (APA)
Jiang, X., Luo, C., Qiang, X., Zhang, Q., Kolstein, H., & Bijlaard, F. (2018). Coupled hygro-mechanical finite element method on determination of the interlaminar shear modulus of glass fiber-reinforced polymer laminates in bridge decks under hygrothermal aging effects. Polymers, 10(8), [845]. https://doi.org/10.3390/polym10080845

Important note
To cite this publication, please use the final published version (if applicable). Please check the document version above.
Coupled Hygro-Mechanical Finite Element Method on Determination of the Interlaminar Shear Modulus of Glass Fiber-Reinforced Polymer Laminates in Bridge Decks under Hygrothermal Aging Effects

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Received: 26 June 2018; Accepted: 25 July 2018; Published: 1 August 2018

Abstract: To investigate the mechanical degradation of the shear properties of glass fiber-reinforced polymer (GFRP) laminates in bridge decks under hygrothermal aging effects, short-beam shear tests were performed following the ASTM test standard (ASTM D790-10A). Based on the coupled hygro-mechanical finite element (FE) analysis method, an inverse parameter identification approach based on short-beam shear tests was developed and then employed to determine the environment-dependent interlaminar shear modulus of GFRP laminates. Subsequently, the shear strength and modulus of dry ($0\% M_t/M_\infty$), moisture unsaturated ($30\% M_t/M_\infty$ and $50\% M_t/M_\infty$), and moisture saturated ($100\% M_t/M_\infty$) specimens at test temperatures of both $20\, ^\circ\mathrm{C}$ and $40\, ^\circ\mathrm{C}$ were compared. One cycle of the moisture absorption–desorption process was also investigated to address how the moisture-induced residual damage degrades the shear properties of GFRP laminates. The results revealed that the shear strength and modulus of moisture-saturated GFRP laminates decreased significantly, and the elevated testing temperature ($40\, ^\circ\mathrm{C}$) aggravated moisture-induced mechanical degradation. Moreover, an unrecoverable loss of shear properties for the GFRP laminates enduring one cycle of the moisture absorption–desorption process was evident.

Keywords: fiber-reinforced polymer composite; interlaminar shear modulus; hygrothermal aging effect; mechanical degradation; short-beam test; finite element method

1. Introduction

Various types of fiber-reinforced polymer (FRP) composites are being used in different fields of application, ranging from sporting goods to structural materials for the automotive, maritime, and aerospace industries. During the past two decades, in the civil engineering field, FRP bridge decks are increasingly being used for the rehabilitation of old concrete–steel composite bridges and the new construction of pedestrian and highway bridges [1–6], due to their various advantages, including [7,8]: a high strength-to-weight ratio, good corrosion resistance, controllable quality, low maintenance cost, and rapid installation with minimum traffic disruption. Although FRP decks are increasingly being used in civil infrastructure applications, their durability and long-term performance are still not comprehensively understood. In such applications, FRP composites are usually exposed to harsh and
variable environments with various temperature and moisture ranges (including elevated temperature immersion and “hot/wet” environment exposures). The “hot/wet” environment exposure is supposed to be the severest environmental condition to degrade the mechanical performance of polymeric materials [9–19], which will consequently deteriorate the long-term performance of FRP composite bridges. A comprehensive understanding of the mechanisms of the hygrothermal aging-related degradation on FRP composite materials is necessary for the purposes of evaluating and predicting the service life and durability of FRP infrastructures. In the literature, the influence of moisture absorption on the mechanical properties of FRP composites is well documented [9–14,17,20–26], regarding the tensile, interlaminar shear, and flexural properties as well as toughness. Generally, the combination of moisture and temperature effects seriously degraded the mechanical properties of FRP composites. Due to this mechanism, overall reductions in the modulus, strength, and glass transition temperature of FRP materials were recorded, which were attributed to the plasticizing effect of water absorbed in the matrix. However, results and conclusions vary with the types of matrix (even fibers), fabrication methods, specimen geometries, curing processes, and service environmental conditions.

In order to keep pace with the application of FRP composites in the civil engineering field, this research was undertaken to reveal more knowledge about the environmental degradation of glass fiber-reinforced polymer (GFRP) composite bridges in hot/wet environments. For the use of GFRP bridge decks, GFRP laminates are mainly loaded by wheels in the through-thickness direction. Therefore, the interlaminar shear properties of GFRP materials are of great importance. Currently, standard test methods exist mostly for determination of the in-plane normal and shear modulus, and the strength parameters of FRP composite materials [27]. However, the test method to directly obtain the interlaminar shear modulus is very limited. Failure always occurred through a combination of shear and transverse tension, indicating that a pure shear failure mode was not evident in the test. Therefore, it is imperative that robust methodologies for determining the interlaminar material properties of FRP materials need to be developed. To achieve this objective, in this research, a coupled hygro-mechanical finite element (FE) modeling method was developed. An inverse parameter identification approach to determine the interlaminar shear modulus G13 (G23) of FRP laminates was established.

Through investigation of the sensitivity of the FE analysis [28], it is concluded that the short-beam three-point bending test (rather than the standard Iosipescu test and off-axis tensile test) is sensitive to changes in the interlaminar shear modulus, but relatively insensitive to changes in the other unknown material properties. Hence, the short-beam three-point bending test is the most suitable method to study the interlaminar shear modulus. Thus, short-beam three-point bending tests were conducted in this research to provide the data base to develop the coupled hygro-mechanical finite element model for numerically determining the interlaminar shear modulus of GFRP laminates, and furthermore to systematically study the influence of moisture and temperature effects on the shear modulus and strength of GFRP laminates.

2. Experiment

2.1. Material

As aforementioned, to obtain the test database of the coupled hygro-mechanical finite element model and investigate the interlaminar shear property of FRP laminates, three-point bending tests of short-beam GFRP specimens are firstly conducted. The whole test procedure follows the test standard ASTM D2344/D2344M-00 [29]. The GFRP laminates studied in this paper were manufactured by resin vacuum infusion (Infra Composite BV, Breukelen, The Netherlands) using polyester, and then cut into specific dimensions (see Figure 1). The Tg (glass transition temperature) of GFRP is 78 °C, and the maximum working temperature could be 63 °C, which is 15 °C lower than Tg.
The 5.64-mm thick specimen is composed of six layers of standard 0.94 mm EQX1200. The layup configuration of each piece of the standard 0.94-mm EQX1200 is illustrated in Table 1, which is a glass fiber-reinforced polymer composite (54% glass content by weight). The mechanical properties of the GFRP laminates supplied by the manufacturer are shown in Table 2. As shown in Table 1, the nominal length and width of the specimens are selected to be 12 mm and 40 mm.

### Table 1. Glass fiber-reinforced polymer (GFRP) laminate properties of EQX1200 (supplied by the manufacturer).

| Product Name | Total Weight (g/m²) | 0° (Warp) | +45° | 90° (Weft) | −45° | Knit Yarn |
|--------------|---------------------|-----------|------|------------|------|-----------|
| EQX 1200     | 1193                | 283       | 300  | 300        | 300  | 10        |

### Table 2. Mechanical properties of GFRP laminates (supplied by the manufacturer).

| Property              | Tensile (ISO 527-4) | Compression (ISO 8515) | Flexural (ISO 14.125) |
|-----------------------|----------------------|------------------------|-----------------------|
| Mean Value            | Warp                 | Weft                   | Warp                  | Weft   |
| Strength              | 331 MPa              | 314 MPa                | 220 MPa               | 200 MPa |
| Modulus               | 18 GPa               | 17 GPa                 | 14 GPa                | 14 GPa  |
|                       |                      |                        | 13 GPa                | 11 GPa  |

#### 2.2. Methodology

The numbering of specimens with regard to the moisture uptake content, test temperature, absorption/desorption process, and replicated number is listed in Table 3. Two test temperatures, 20 °C and 40 °C, are proposed for the short-beam three-point bending tests, which are controlled by a climate chamber with the tolerance of ±2 °C, as shown in Figure 2. During the short-beam tests, a temperature sensor is attached to the tested GFRP specimen. The test is conducted when the temperature of the specimen reaches the proposed value.

### Table 3. GFRP laminate specimens for short-beam shear tests.

| Specimen Identification | Test | M₀/M∞ | Test Temperature | After Desorption | Number of Specimens |
|-------------------------|------|-------|------------------|------------------|--------------------|
| Set-1                   | shear| 0     | 20 °C            | no               | 5                  |
| Set-2                   | shear| 0     | 40 °C            | no               | 5                  |
| Set-3                   | shear| 30%   | 20 °C            | no               | 5                  |
| Set-4                   | shear| 30%   | 40 °C            | no               | 5                  |
| Set-5                   | shear| 50%   | 20 °C            | no               | 5                  |
| Set-6                   | shear| 50%   | 40 °C            | no               | 5                  |
| Set-7                   | shear| 100%  | 20 °C            | no               | 5                  |
|                         |      | 100%  | 40 °C            | no               | 5                  |
|                         | shear| 50%   | 20 °C            | yes              | 5                  |
|                         |      | 50%   | 40 °C            | yes              | 5                  |
|                         | shear| 30%   | 20 °C            | yes              | 5                  |
|                         |      | 30%   | 40 °C            | yes              | 5                  |
|                         | shear| 0     | 20 °C            | yes              | 5                  |
|                         |      | 0     | 40 °C            | yes              | 5                  |
The Set-3 specimens (S-50%-20 °C) are tested at the 50% relative moisture uptake content. The Set-4 specimens (S-100%-20 °C and S-100%-40 °C) are tested at the moisture saturation level (100% relative moisture uptake content), and the above test series is considered as the moisture absorption process. Then, the rest specimens are all taken out of the hygrothermal aging environment, and put into an oven at a temperature of 42 °C to be dried. This is considered the moisture desorption process. In this way, the Set-5 specimens (S-50%-20 °C-D and S-50%-40 °C-D) are tested at 50% relative moisture uptake content after a certain time of moisture desorption. Subsequently, the Set-6 specimens (S-30%-20 °C-D and S-30%-40 °C-D) are tested at 30% relative moisture uptake content after the moisture desorption. The Set-7 specimens (S-0-20 °C-D and S-0-40 °C-D) are the fully dry specimens after one cycle of the moisture absorption–desorption process.

The moisture uptake content of each specimen is recorded by using the gravimetric test method [30]. The moisture uptake content \( (w_t) \) of each specimen is calculated according to its weight before exposure \( (w_0) \) and after exposure \( (w_t) \) as follows:

\[
M_t = 100 \times \left( \frac{w_t - w_0}{w_0} \right) 
\]

(1)

Figure 2. Climate chamber during short-beam tests.

As listed in Table 3, the test under each condition is repeated five times to investigate the deviation of test results. The hygrothermal aging condition (40 °C-water) is supposed to be a relatively severe hot/wet condition for GFRP laminates, as stated in previous research [30]. In total, 70 pieces of specimens are prepared. During the hygrothermal aging procedure, all of the specimens are immersed in water at a temperature of 40 °C, except for the S-0-20 °C and S-0-40 °C specimens, which are the as-received reference specimens (Set-1 in Table 3). The as-received specimens are stored in the laboratory environment. As measured after the moisture desorption, the moisture contents of the specimens are approximately zero. For the other specimens (as illustrated in Table 3), the Set-2 specimens (S-30%-20 °C and S-30%-40 °C) are tested at the 30% relative moisture uptake content. The Set-3 specimens (S-50%-20 °C and S-50%-40 °C) are tested at the 50% relative moisture uptake content. The Set-4 specimens (S-100%-20 °C and S-100%-40 °C) are tested at the moisture saturation level (100% relative moisture uptake content), and the above test series is considered as the moisture absorption process. Herein, the symbol “D” indicates moisture desorption. During the whole aging procedure, the moisture uptake content of each specimen is recorded by using the gravimetric test method [30]. The moisture uptake content \( (Mt) \) of each specimen is calculated according to its weight before exposure \( (w_0) \) and after exposure \( (w_t) \) as follows:

\[
M_t = 100 \times \left( \frac{w_t - w_0}{w_0} \right) 
\]

The short-beam shear test device is shown in Figure 3.
According to ASTM D2344/D2344M-00 [29], the loading span length-to-specimen thickness ratio is four. Consequently, the support span is proposed to be 22.6 mm. It varies among different groups of specimens, since the value of the support span is exactly calculated based on the average thickness of each specimen group. The diameter of the loading nose and supports are 6.00 mm and 3.00 mm, respectively. The crosshead movement speed of testing is set at a rate of 1.0 mm/min. The specimen is deflected until the load drops to 30% of the maximum load or until a maximum displacement of mid-span reaches 4 mm (see Figure 4). The experimental data is recorded per second.

According to the test standard ASTM D2344/D2344M-00 [29], the short-beam shear strength of the FRP laminates can be calculated as follows:

\[ F_{sbs} = 0.75 \times \frac{P_m}{b \times h} \]  

(2)

where:

- \( F_{sbs} \) = short-beam strength, MPa,
- \( P_m \) = maximum load observed during the test, N,
- \( b \) = measured specimen width, mm,
- \( h \) = measured specimen thickness, mm.

Figure 3. Short-beam shear test device.

Figure 4. Termination rule for the short-beam shear test. (a) Drop to 30% of the maximum load; (b) Maximum displacement of 4 mm.
3. Experimental Results and Discussion

Figure 5 shows the moisture absorption process (red points) of GFRP short-beam specimens immersed in water of 40 °C. Moisture content ($M_t$) is drawn as the function of square root of time. It can be found that the moisture saturation level is about 0.72%.

![Figure 5. Comparison of moisture uptake curve between test results and finite element (FE) analysis on FRP specimens for short-beam shear tests.](image)

The typical failure mode of short-beam shear specimens is shown in Figure 6, which is the interlaminar failure through the thickness of GFRP laminates.

![Figure 6. Failure mode of the short-beam shear test specimen.](image)

Figure 7 shows the mechanical degradation on short-beam shear strength of FRP laminates as a function of moisture uptake content at the test temperatures of 20 °C and 40 °C, respectively.
Predictive equations for the short-beam shear strength degradation as the function of moisture content is curve-fitted by the exponential function using the least square method. They are as follows:

20 °C, absorption process:

\[ S = 5.5 \left( \frac{M_t}{M_\infty} \right)^{-1.76} + 11 \]  
(3)

20 °C, absorption–desorption process:

\[ S = 34 \left( \frac{M_t}{M_\infty} \right)^{-0.517} + 14.4 \]  
(4)
$40^\circ C$, absorption process:

$$S = 9.6^{-\left(\frac{M_t}{M_\infty} - 1.28\right)} + 12$$

(5)

$40^\circ C$, absorption–desorption process:

$$S = 46.8^{-\left(\frac{M_t}{M_\infty} - 0.45\right)} + 13.6$$

(6)

All of the predictive curves are illustrated in Figure 7 for comparison with the experimental results. The R-square values of each curve are also present in Figure 7, which indicates the accuracy of curve fitting on test data points.

As shown in Figure 7a, in the moisture absorption process, the short-beam shear strength is quasi-linearly decreasing from the fully dry specimens to the specimens with about 75% moisture uptake content of the saturated level. Then, test data points distribute stably until reaching the moisture saturated condition (100% $M_\infty$). As listed in Table 4, the short-beam shear strength of the moisture saturated specimens is 15 MPa, which is 53.1% lower than that of the fully dry specimens (32 MPa).

Table 4. Short-beam shear strength degradation of FRP laminates.

| Specimen Identification | Shear Strength * (MPa) | Standard Deviation (MPa) |
|-------------------------|------------------------|--------------------------|
| S-0%-20 °C              | 32                     | 2.74                     |
| S-0%-40 °C              | 31                     | 1.34                     |
| S-30%-20 °C             | 26                     | 1.70                     |
| S-30%-40 °C             | 25                     | 1.89                     |
| S-50%-20 °C             | 19                     | 0.59                     |
| S-50%-40 °C             | 16                     | 2.10                     |
| S-100%-20 °C            | 15                     | 0.24                     |
| S-100%-40 °C            | 14                     | 0.41                     |
| S-50%-20 °C-D           | 15                     | 1.08                     |
| S-50%-40 °C-D           | 13                     | 0.41                     |
| S-30%-20 °C-D           | 16                     | 0.76                     |
| S-30%-40 °C-D           | 15                     | 0.21                     |
| S-0%-20 °C-D            | 21                     | 0.35                     |
| S-0%-40 °C-D            | 19                     | 0.36                     |

* mean value of five specimens.

Furthermore, in the moisture absorption process, the test data points are distributed more dispersively, since the moisture uptake process deviates significantly for small scale short-beam specimens. It can be due to the reason that, under the same water aging time, the moisture uptake contents of the individual specimens differ from each other within a certain range. The extent of mechanical degradation is closely related to the moisture content of FRP specimens, but is not related to the aging time.

As for the moisture desorption process, from the saturated condition to the fully dry condition, the short-beam shear strength is slightly increasing, and ends at 21 MPa. It is 34.4% lower than that of the unconditioned dry specimens. This means that one cycle of the moisture absorption–desorption process deteriorated the shear strength of FRP laminates by 34.4% permanently.

Figure 7b presents the same tendency regarding the degradation of the short-beam shear strength of GFRP laminates at 40 °C. As listed in Table 4, the higher temperature (40 °C) only slightly deteriorates the shear strength of GFRP specimens, which implies that the influence of temperature is not as significant as the influence of moisture.
4. Coupled Hygro-Mechanical FE Method on Determination of the Interlaminar Shear Modulus of FRP Laminates

For the coupled hygro-mechanical FE method, it is realized in the following steps. The first step is modeling moisture transport through FRP structures in order to determine the moisture concentration distribution across the cross-sections as a function of time. The material parameters required for the transient diffusion FE analysis are moisture diffusion coefficients and solubility, which can be obtained from short-term gravimetric experiments, as stated in previous research [30]. From the moisture diffusion analysis, the moisture concentration distribution across the FRP section can be read into the stress analysis as a predefined field variable. Then, the environment-dependent mechanical behavior of FRP structures can be investigated using the FE stress–strain analysis based on this predefined field. The input moisture-dependent material properties of FRP composites are obtained by material tests (such as flexural test, tensile test, and short-beam shear test).

In this research, the FE modeling is conducted by employing the FE software ABAQUS. Firstly, the moisture diffusion process of the short-beam GFRP specimen (FE model is shown in Figure 8) is simulated using the transient-field FE diffusion analysis. The type of finite elements is C3D8R. The GFRP material is modeled as an orthotropic material. Moisture diffusion coefficients in three directions are input as $D_1 = 9.607 \times 10^{-6}$ mm$^2$/s, $D_2 = 9.631 \times 10^{-6}$ mm$^2$/s, and $D_3 = 0.318 \times 10^{-6}$ mm$^2$/s (40 °C-water aging condition), which are obtained from the previous research [30].

From Figure 5, good agreement is evident between the experimental results and FE simulation. From the transient-field FE moisture diffusion analysis, the moisture concentration distribution across the short-beam GFRP specimen section is obtained as a function of time, which can be read into the following stress–strain analysis as a predefined field variable at different time intervals. To determine the environment-dependent interlaminar shear modulus of FRP laminates, the coupled hygro-mechanical FE modeling method is employed herein, which was already well developed and validated by flexural tests in the previous research [31]. For instance, at the test temperature of 20 °C and during the moisture absorption process, the flexural modulus (E11 and E22) of GFRP laminates with a nominal moisture content ($M_t$) from 0% to 100% can be calculated using the predictive equations (available in the Ref. [31] of Jiang et al.). It is employed as field-dependent input values for material properties of the FE model herein, which means the flexural modulus of each element is determined by the local moisture concentration. Other material properties are determined according to Table 5, which is supplied by the manufacturer. Depending on the sensitivity analysis, determination of the interlaminar shear modulus is not sensitive to the variation of these material properties. Consequently, the interlaminar shear modulus of GFRP laminates is determined by fitting the coupled hygro-mechanical FE analysis results to the short-beam shear test data.

| Property | FRP Laminates |
|----------|---------------|
| E$_{33}$ (MPa) | 11,000 |
| $v_{12}$ | 0.33 |
| $v_{23}$ | 0.3 |
| $v_{13}$ | 0.18 |
| G$_{12}$ (MPa) | 6986 |
According to the test standard ASTM D790-10 [32], as illustrated in Figure 9, the initial non-linear stage of test results is an artifact caused by a take-up of slackness and realignment of the specimens, which does not represent the properties of FRP material. In order to obtain correct values for the material properties, this curve must be offset to the corrected zero point (point B in Figure 9). For each test, the initial non-linear regions are different from each other. To make easy comparisons, all of the experimental curves are offset from B to A, to make the extension line of the linear CD region exactly through the zero point of the coordinates.

Furthermore, it is assumed that degradation of interlaminar shear modulus follows a linear relationship with nominal moisture content, which has the same tendency as that obtained from the flexural modulus of GFRP laminates [31]. Subsequently, the interlaminar shear modulus of GFRP specimens with 0% moisture content (S-0%-20 °C) is firstly determined by fitting the FE load–deflection curve to test results, as shown in Figure 10a. Accordingly, the shear modulus G13 (G23) is numerically determined as 1200 MPa. In the same way, the shear modulus G13 (G23) of GFRP specimens with the 100% moisture content (S-100%-20 °C) is determined as 800 MPa (Figure 10b).
The predictive equation for the interlaminar shear modulus of FRP laminates at the test temperature of 20 °C and during the moisture absorption process can be gained as follows:

\[ G_{23} = G_{13} = -\frac{400 \times M_t}{M_{\infty}} + 1200 \]  

(7)

To validate Equation (7), the other two exposure time intervals (30% \( M_t/M_{\infty} \) and 50% \( M_t/M_{\infty} \)) are employed. As aforementioned, the moisture diffusion process of the FRP specimen is firstly modeled by the transient-field FE diffusion analysis. According to the moisture diffusion analysis, the moisture concentration distributions across the mid-plane of the FRP specimens are presented in Figures 11 and 12, which are used as the input field for the coupled hygro-mechanical analysis. The field-dependent shear modulus is input as calculated by Equation (7).

**Figure 10.** Comparison of load–deflection curves between FE analysis and test results of S-0%-20 °C specimens and S-100%-20 °C specimens.

**Figure 11.** Moisture concentration distribution across the mid-plane of the GFRP specimen with 30% moisture uptake content (time = 26 h).
Figure 12. Moisture concentration distribution across the mid-plane of the GFRP specimen with 50% moisture uptake content (time = 107 h).

Comparison between FE results and test data of S-30%-20 °C specimens and S-50%-20 °C specimens is shown in Figure 13a,b respectively. Good agreements on the slopes of load-displacement curves are achieved for these two groups of specimens, which prove that the predictive Equation (7) is relatively accurate to simulate the stiffness of GFRP specimens with other moisture contents.

Figure 13. Comparison of load–deflection curves between FE analysis and test results of S-30%-20 °C specimens and S-50%-20 °C specimens.
For the GFRP specimens tested at 20 °C and during the moisture desorption process, the same inverse parameter identification method is employed to determine the environment-dependent interlaminar shear modulus of FRP laminates. The predictive equation is fitted and validated by the middle two exposure time intervals (unsaturated conditions 30% and 50%), as follows:

$$G_{23} = G_{13} = -\frac{50 \times M_t}{M_{\infty}} + 850$$  \hspace{1cm} (8)

For the FRP specimens tested at 40 °C and in the moisture absorption process, the predictive equation is as follows:

$$G_{23} = G_{13} = -\frac{450 \times M_t}{M_{\infty}} + 1050$$  \hspace{1cm} (9)

For the FRP specimens tested at 40 °C and in the moisture desorption process, the predictive equation is as follows:

$$G_{23} = G_{13} = -\frac{250 \times M_t}{M_{\infty}} + 850$$  \hspace{1cm} (10)

For easy comparison, the stiffness of specimens is listed in Table 6, which are the slopes of load–deflection curves for the test and FE results. As shown in Table 5 and Figures 14–16, a good agreement on the stiffness of specimens is evident between the FE predicted curves and test results. However, there are some exceptions (S-50%-20 °C-2, S-50%-20 °C-4, S-50%-40 °C-2, and S-50%-40 °C-4 specimens), which significantly deviate from other specimens in the same test group. It can be attributed to the non-homogeneity of GFRP laminate specimens, which influence the stiffness of the material. It also influences the moisture absorption property (different moisture content at the same aging time), and correspondingly degrades the material stiffness. Excluding these exceptions, predictive equations of moisture-dependent interlaminar shear modulus are acceptably reliable. Hence, they can be employed as input material properties of a hygro-mechanical FE model to analyze the environment-dependent mechanical behaviors of complex FRP components, joints, and structures in the future works.

Figure 14. Cont.
Figure 14. Comparison of load–deflection curves between FE analysis and test results of specimens tested at 20 °C and in the moisture desorption process.

Figure 15. Comparison of load–deflection curves between FE analysis and test results of specimens tested at 40 °C and in the moisture absorption process.
Figure 16. Comparison of load–deflection curves between FE analysis and test results of specimens tested at 40 °C and in the moisture desorption process.

Table 6. Stiffness of specimens based on load–deflection curves (Unit: N/mm). FEM: finite element method.

| Specimen Identification | Identification | Mean Value | FEM | Error (100%) |
|-------------------------|----------------|------------|-----|--------------|
| S-0%-20 °C             | 4582 4323 3973 4337 4534 | 4350 | 4286 | 1.47 |
| S-30%-20 °C            | 3535 3692 3682 4318 3878 | 3821 | 4027 | 5.39 |
| S-50%-20 °C            | 3659 3981 4062 3840 3684 | 3845 | 3896 | 1.32 |
| S-100%-20 °C           | 3185 3163 3223 3556 2355 | 3096 | 3333 | 7.64 |
| S-0%-20 °C-D           | 3295 3374 3696 3154 3919 | 3488 | 3571 | 2.39 |
| S-30%-20 °C-D          | 3530 3426 3175 3178 3212 | 3304 | 3529 | 6.80 |
| S-50%-20 °C-D          | 3632 2865 3405 2506 3517 | 3185 | 3448 | 8.26 |
| S-0%-40 °C             | 3864 4162 3692 3919 4129 | 3953 | 3797 | 3.95 |
| S-30%-40 °C            | 3938 4320 3824 4287 3753 | 4024 | 3488 | 8.36 |
| S-50%-40 °C            | 4044 3069 3518 2286 3187 | 3221 | 3409 | 5.84 |
| S-100%-40 °C           | 2897 2986 2588 3073 2694 | 2830 | 2778 | 1.82 |
| S-0%-40 °C-D           | 2831 2661 2583 2653 2758 | 2697 | 2970 | 2.70 |
| S-30%-40 °C-D          | 2664 2916 2902 2898 2587 | 2793 | 3125 | 8.29 |
| S-50%-40 °C-D          | 2831 2661 2583 2653 2758 | 2697 | 2970 | 6.41 |

Figure 17 illustrates the degradation tendency of the interlaminar shear modulus of FRP laminates due to moisture diffusion and temperature. For the specimens tested at 20 °C, a dramatic drop on interlaminar shear modulus is found from the unconditioned dry specimen (1200 MPa) to the
moisture-saturated specimen (800 MPa). After the moisture desorption process, a slight recovery is found for the shear modulus of S-0%-20 °C-D specimens (850 MPa). In total, a 29.2% decrease of interlaminar shear modulus is obtained for the specimens enduring one cycle of the moisture absorption–desorption process. For the specimens tested at 40 °C, a similar tendency of interlaminar shear modulus loss is obtained, with a 42.9% decrease from the unconditioned dry specimens (1050 MPa) to the saturated specimens (600 MPa), and a 19% decrease for the specimens enduring one cycle of the moisture absorption–desorption process.

![Graph showing degradation on interlaminar shear modulus](image)

**Figure 17.** Degradation on the interlaminar shear modulus of GFRP laminates.

### 5. Conclusions

This paper describes the investigations on the environment-dependent shear properties of GFRP laminates and the coupled hygro-mechanical FE method. Detailed conclusions can be drawn as follows:

1. The short-beam shear strength of the moisture-saturated specimens tested at 20 °C is 15 MPa, which is 53.1% lower than that of the unconditioned dry specimens (32 MPa). One cycle of the moisture absorption–desorption process degraded the shear strength of GFRP laminates by 34.4%.
The elevated test temperature (40 °C) did not significantly degrade the shear strength of the GFRP laminates with different moisture contents.

2. Based on the coupled hygro-mechanical FE analysis method, an inverse parameter identification approach to short-beam shear tests was developed and employed to determine the environment-dependent interlaminar shear modulus of GFRP laminates. This method was proven to be effective to determine the interlaminar shear modulus of FRP materials.

3. Compared with the unconditioned dry specimen, the interlaminar shear modulus of the moisture-saturated specimen tested at 20 °C and 40 °C decreased by 33.3% and 42.9%, respectively. One moisture absorption-desorption process induced a 29.2% loss of interlaminar shear modulus for specimens tested at 20 °C, and a 19% loss for specimens tested at 40 °C.

4. Predictive equations for moisture-dependent shear strength and the modulus of GFRP laminates were obtained in this research. These predictive equations can be used as input parameters for a coupled hygro-mechanical FE model, and contribute to the design code of FRP structures as far as the long-term performance is concerned.

Author Contributions: X.J. conceived and designed the test setup and experiments. C.L. performed the experiments. X.J. and X.Q. analyzed the test data. X.Q. did the finite element analysis. X.J. and X.Q. co-wrote the paper. Q.Z. and X.J. revised the paper. H.K. and F.B. supervised the whole research process, and organized the works related to the experiments.

Funding: The research is funded by the National Natural Science Foundation of China (Program No. 51408424, 51578404), the Fundamental Research Funds for the Central Universities of China and Infra Composites B.V.

Acknowledgments: The authors would like to thank the National Natural Science Foundation of China (Program No. 51408424, 51578404), the Fundamental Research Funds for the Central Universities of China and Infra Composites B.V. for financial support and supplying GFRP laminates of this research.

Conflicts of Interest: The authors declare no conflict of interest.

References

1. Knippers, J.; Pelke, E.; Gabler, M.; Berger, D. Bridges with Glass Fibre-Reinforced Polymer Decks: The Road Bridge in Friedberg, Germany. *Struct. Eng. Int.* 2010, 20, 400–404. [CrossRef]

2. Luke, S.; Canning, L.; Collins, S.; Knudsen, E.; Brown, P.; Taljsten, B.; Olofsson, I. Advanced composite bridge decking system—Project ASSET. *Struct. Eng. Int.* 2002, 12, 76–79. [CrossRef]

3. Alampalli, S.; Kunin, J. Rehabilitation and field testing of an FRP bridge deck on a truss bridge. *Compos. Struct.* 2002, 57, 373–375. [CrossRef]

4. Schollmayer, M. *Through-Thickness Performance of Adhesive Connections between FRP Bridge Decks and Steel Main Girders*; Ecole Polytechnique Federale de Lausanne: Lausanne, Switzerland, 2009.

5. Gurtler, H.W. *Composite Action of FRP Bridge Decks Adhesively Bonded to Steel Main Girders* Lausanne; Ecole Polytechnique Federale de Lausanne: Lausanne, Switzerland, 2004.

6. Keller, T.; Bai, Y.; Vallee, T. Long-term performance of a glass fiber-reinforced polymer truss bridge. *J. Compos. Constr.* 2007, 11, 99–108. [CrossRef]

7. Hollaway, L.C. A review of the present and future utilisation of FRP composites in the civil infrastructure with reference to their important in-service properties. *Constr. Build. Mater.* 2010, 24, 2419–2445. [CrossRef]

8. Awad, Z.K.; Aravinthanam, T.; Zhuge, Y.; Gonzalez, F. A review of optimization techniques used in the design of fibre composite structures for civil engineering applications. *Mater. Des.* 2012, 33, 534–544.

9. Shao, Y.X.; Kouadi, S. Durability of fiberglass composite sheet piles in water. *J. Compos. Constr.* 2002, 6, 280–287. [CrossRef]

10. Bank, L.C.; Gentry, T.R.; Barkatt, A. Accelerated Test Methods to Determine the Long-Term Behavior of Frp Composite Structures–Environmental-Effects. *J. Reinf. Plast. Compos.* 1995, 14, 559–587. [CrossRef]

11. Nogueira, P.; Ramirez, C.; Torres, A.; Abad, M.J.; Cano, J.; Lopez, J.; Barral, L. Effect of water sorption on the structure and mechanical properties of an epoxy resin system. *J. Appl. Polym. Sci.* 2001, 80, 71–80.

12. Earl, J.S.; Shenoi, R.A. Hygrothermal ageing effects on FRP laminate and structural foam materials. *Compos. Part A Appl. Sci. Manuf.* 2004, 35, 1237–1247. [CrossRef]
13. Robert, M.; Roy, R.; Benmokrane, B. Environmental Effects on Glass Fiber Reinforced Polypropylene Thermoplastic Composite Laminate for Structural Applications. *Polym. Compos.* **2010**, *31*, 604–611. [CrossRef]

14. Karbhari, V.M. E-glass/vinylester composites in aqueous environments: Effects on short-beam shear strength. *J. Compos. Constr.* **2004**, *8*, 148–156. [CrossRef]

15. Daly, H.B.; Brahim, H.B.; Hfiaied, N.; Harchay, M.; Boukili, R. Investigation of water absorption in pultruded composites containing fillers and low profile additives. *Polym. Compos.* **2007**, *28*, 355–364. [CrossRef]

16. Karbhari, V.M.; Xian, G.J. Hygrothermal effects on high VF pultruded unidirectional carbon/epoxy composites: Moisture uptake. *Compos. Part B Eng.* **2009**, *40*, 41–49. [CrossRef]

17. Yilmaz, T.; Sinmazcelik, T. Effects of hydrothermal aging on glass–fiber/polyetherimide (PEI) composites. *J. Mater. Sci.* **2010**, *45*, 399–404. [CrossRef]

18. Jiang, X.; Kolstein, H.; Bijlaard, F.S.K. Moisture diffusion and hygrothermal aging in pultruded fibre reinforced polymer composites of bridge decks. *Mater. Des.* **2012**, *37*, 304–312. [CrossRef]

19. Shi, S.; Gu, L.; Liang, J.; Fang, G.; Gong, C.; Dai, C. A mesomechanical model for predicting the degradation in stiffness of FRP composites subjected to combined thermal and mechanical loading. *Mater. Des.* **2016**, *89*, 1079–1085. [CrossRef]

20. Springer, G.S. *Environmental Effects on Composite Materials*, Vol.1; Technomic Publishing Company: Lancaster, PA, USA, 1981.

21. Springer, G.S. *Environmental Effects on Composite Materials*, Vol.2; Technomic Publishing Company: Lancaster, PA, USA, 1984.

22. Springer, G.S. *Environmental Effects on Composite Materials*, Vol.3; Technomic Publishing Company: Lancaster, PA, USA, 1987.

23. Loh, W.K.; Crocombe, A.D.; Wahab, M.M.A.; Ashcroft, I.A. Modelling anomalous moisture uptake, swelling and thermal characteristics of a rubber toughened epoxy adhesive. *Int. J. Adhes. Adhes.* **2005**, *25*, 1–12. [CrossRef]

24. Haque, A.; Mahmood, S.; Walker, L.; Jeelani, S. Moisture and Temperature Induced Degradation in Tensile Properties of Kevlar Graphite Epoxy Hybrid Composites. *J. Reinf. Plast. Compos.* **1991**, *10*, 132–145. [CrossRef]

25. Akay, M.; Mun, S.K.A.; Stanley, A. Influence of moisture on the thermal and mechanical properties of autoclaved and oven-cured Kevlar-49/epoxy laminates. *Compos. Sci. Technol.* **1997**, *57*, 565–571. [CrossRef]

26. Esfahani, S.; Honarbaksh-Raouf, A.; Esfahani, S. Effects of moisture absorption on degradation of E-glass fiber reinforced Vinyl Ester composite pipes and modelling of transient moisture diffusion using finite element analysis. *Corros. Sci.* **2015**, *90*, 168–175. [CrossRef]

27. Staab, G.H. *Laminar Composites*; Butterworth-Heinemann: Oxford, UK, 1999.

28. Chan, A.; Chiu, W.K.; Liu, X.L. Determining the elastic interlaminar shear modulus of composite laminates. *Compos. Struct.* **2007**, *80*, 396–408. [CrossRef]

29. ASTM D2344/2344M-00. *Standard Test Methods for Short-Beam Strength of Polymer Matrix Composite Materials and Their Laminates*; ASTM International: West Conshohocken, PA, USA, 2000.

30. Jiang, X.; Kolstein, H.; Bijlaard, F.; Qiang, X.H. Effects of hygrothermal aging on glass-fiber reinforced polymer laminates and adhesive of FRP composite bridge: Moisture diffusion characteristics. *Compos. Part A Appl. Sci. Manuf.* **2014**, *57*, 49–58. [CrossRef]

31. Jiang, X.; Song, J.; Qiang, X.; Kolstein, H.; Bijlaard, F. Moisture Absorption/Desorption Effects on Flexural Property of Glass-Fiber-Reinforced Polyester Laminates: Three-Point Bending Test and Coupled Hygro-Mechanical Finite Element Analysis. *Polymers* **2016**, *8*, 290. [CrossRef]

32. ASTM D790-10. *Standard Test Methods for Flexural Properties of Unreinforced and Reinforced Plastics and Electrical Insulating Materials*; ASTM International: West Conshohocken, PA, USA, 2010.