Chirality transitions in a system of active flat spinners

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We study in this work the 2D dynamics of an experimental system of disk-shaped rotors, fluidized by turbulent upflow. Contrary to previous knowledge, our experiments show the same particle chiral geometry can produce flows with different chiralities. In particular, we unveil a conspicuous complex chiral flow, which displays multiple persistent vortexes with either sign, located randomly in the system. This peculiar phase mediates a continuous transition, which takes place as the kinetic energy input increases, from a flow with positive chirality (one vortex rotating in the same direction as particles spin) to a flow with negative chirality (one vortex in opposite sense to particle spin). We find that these surprising transitions are determined by the specific state of the statistical correlations between particle spin and translational velocity. We discuss how these correlations are determined in turn by the combined action of a series of mechanisms (for instance, heat dissipation at the boundaries, particle activity, average kinetic energy...), several of which are unveiled here.

I. INTRODUCTION

Chiral fluids have received much attention in recent years due to their complex and non-trivial dynamics. Examples can be found in a variety of contexts and scales: biology [1], colloids [2], granular matter [3], etc. These chiral fluids are all composed of many particles with some kind of geometric or dynamic asymmetry, which breaks the system symmetry under parity and temporal inversion, i.e., they are composed of particles whose geometrical/dynamical configuration has chirality.

An important consequence of this chirality is that hydrodynamic theory for conventional fluids does not describe the complex behavior observed in these fluids. This is so, mainly, because an anti-symmetric component of the stress tensor (absent in regular fluids) emerges in fluids composed of chiral particles. It is well established [4] that the anti-symmetric stress is responsible for the development of chiral flow, which in turn can allow for the emergence of hyperuniform structures [5 6], collective phenomena [7] such as flocking or swarms [8] or topological effects [9]. Therefore, understanding and control of the parameters that govern the complex dynamics of these special fluids can help deepen the knowledge of important biological processes and also allow for the development of applications, such as smart materials [9 10]. However, the mechanisms that, at mesoscopic level, give rise to the emergence of specific properties of this anti-symmetric tensor (which is related to new transport coefficients [11]) are not well understood yet, and as a consequence, the topology of chiral flow is usually analyzed according to the geometrical configuration of particles alone. For instance, the role of the fluidization state of the system and its statistical correlations remains to be determined.

In order to analyze this important question, we study the statistical properties in a set of macroscopic flat spinners, which can be regarded as a simple test system that can reproduce some important aspects of the dynamics in more complex set-ups composed of active rotor particles [2 8 12 14]. Active spinners are relevant since they allow to study a variety of phenomena such as chiral crystals [13], hexatic phase [10], discontinuous chiral flow transition under density changes [17], special topological properties [1 9 18 19], or ferromagnetically coupled rotation [20].

More specifically, and in order to describe the dynamics of chiral particles for a system that is more akin to biological systems, we conduct here an investigation on the phase behavior of a system of flat rotors with constant sign of their average spin (i.e., constant particle chirality sign). In nature, as it is known, most active particles have a definite chemical/geometrical configuration; i.e., the chirality of most active particles is well defined and does not change. And this is actually very relevant since, for instance, many isomers that differ only in the chirality sign play significantly different roles in the most relevant bio-chemical and bio-physical processes, according to particle chirality alone [21].

In several previous works, an important phenomenology of spontaneous changes in the direction of vortex rotations (i.e., inversion of the chirality of the flow) has
been observed \cite{22,25}. However, this inversion appears to be always related to different inversion mechanisms of the chirality of the constituent particles. In effect, inversion of the chirality of the flow has been reported for particles with oscillating/random chirality such as magnetic spinners \cite{22} and rollers \cite{23}, and for Janus particles \cite{24}. Another similar but not analogous situation has been described where, at constant particle chirality sign, centripetal flow rings with alternating vorticity sign appear \cite{24} (and thus, the system does not display actual chiral vortices but opposing alternate stream lines). In summary, according to previous knowledge, a system of particles with inherently constant chirality sign (as ours is) would not have the ability to display chiral flow inversion. As an exception, the flow chirality does not rely on particle chirality inversion, in a recent work \cite{17}. However, flow chirality inversion was produced exclusively under a change in the particle density of the system. We will see that the phenomenology is actually more complex, and a plethora of transitions at constant density are here. We discuss this due to the fact that transitions are controlled by additional variables, found. Furthermore, identification of all the relevant mechanisms in the chiral transitions will allow us to discover a new phase and also previously unknown properties of chiral flow transitions.

Our results reveal that, contrary to what would be expected, inversion of flow chirality for a system of particles with constant chirality sign is possible and is in general to be expected. Furthermore, we have observed that the inversion appears as a continuous transition that is mediated by a complex chiral flow phase (that had remained unknown so far). This complex chiral state is characterized by a disordered spatial distribution of vortexes of different signs and sizes. Moreover, the transition to a flow with reverse chirality sign (i.e., flow chirality is opposed to particle chirality) occurs when the average translational kinetic energy of the particles is above a threshold. Furthermore, the location of this threshold is determined by structural changes in the statistical correlations of the system, whose role has not previously been reported in flow chirality transitions (and that here we characterize by means of a theoretical analysis, based on the description of the cumulants of the single particle distribution function, which have not previously reported in this context either).

II. EXPERIMENTAL SET-UP

We use an experimental configuration consisting of a set of \( N \) identical, flat (disk-shaped) particles which are provided with 14 blades, as sketched in Figure 1(a). The dynamics in our experiments is constrained to a horizontal perforated metallic grid. The grid is delimited by a circular boundary of diameter \( \Delta = 10\sigma \) where \( \sigma = 7.25 \text{ cm} \) is the particle diameter. Particle mass is \( m_p = 7.1 \text{ g} \) and \( I \simeq (1/8) m_p \sigma^2 = 46 \text{ g cm}^2 \) is the moment of inertia (approximating the true value of \( I \) to that of a homogeneous cylinder/disk). A controllable air current impinges the arena from below.

The blades are tilted with respect to the horizontal so that a steady clockwise average spin results from the upflow past the particles (Figure 1(a) that in turn yields vortex shedding \cite{20}, thus inducing stochastic horizontal translations as well. Therefore, under steady air upflow, the system achieves a stationary state with constant (rotational and translational) average particle kinetic energy.

The average kinetic energy of the particles is monotonically increasing for higher air upflow, as Figure 1(b) shows. Due to particle-particle collisions and upflow turbulence, the particle spin \( \mathbf{w} = w_z \hat{e}_z \) is not exactly constant. Here, \( \hat{e}_z \) is a unit vertical vector pointing upwards (same direction, opposite sense of gravity), so that \( w_z < 0 \) stands for clockwise rotation and vice versa. Due to the designed blade tilting in the set of identical disks, \( w_z < 0 \) most times for all particles.

As a consequence of these features, the system displays a non-equilibrium distribution function \( f \), which for an arbitrary state is \( f(r, \mathbf{v}, \mathbf{w}; t) \) (\( t \) is time, \( r \) is the 2D position vector, \( \mathbf{v} \) is particle translational velocity) whose standard deviations depend on air current intensity.

Moreover, as a result of the interplay of particle collisions and air upflow and, due to the symmetries in the experimental set-up, the steady base states (i.e., the simplest steady states \cite{27}) are statistically characterized by a particle distribution function of the form \( f(r, \mathbf{v}, \mathbf{w}) \). Moreover, the geometric asymmetry of the particles (Figure 1(a) yields a non-vanishing spin field of the form \( \Omega(r) = \Omega(r) \hat{e}_z \), which will be responsible for the emergence of circulating flow of the form \( \mathbf{u} = u(r) \hat{e}_\phi \), where \( \hat{e}_\phi \) denotes the azimuthal direction.

In this way, a symmetry break arises so that the flow has chirality \cite{28}.

The marginal distribution functions, used in Figure 1 are defined as

\[
\begin{align*}
& f_{r,w}(v) = \int \left( 1/n(r) \right) dr \int dw f(r, \mathbf{v}, \mathbf{w}) \delta(|v - v'|), \\
& f_{r,u}(w) = \int \left( 1/n(r) \right) dr \int dv f(r, \mathbf{v}, \mathbf{w}) \delta(w_z - w),
\end{align*}
\]

where \( n(r) \) is the particle density field. The relevant fields, particle density \( n(r) \), flow velocity \( \mathbf{u}(r) \), particle average spin \( \Omega(r) \) are defined in Eqs. A3 of Appendix A.2

III. CHIRALITY TRANSITIONS

Since the sign of our particles chirality (spin) is constant, we could only expect, from previous knowledge, that the chiral fluid displays steady flows with a chirality sign that mimics that of its constituent particles, as modelled in theoretical works \cite{4} and extensively reported in previous experiments. (We can only find one previous work where a transition in the sign is reported for particle...
FIG. 1. (a) Schematic renderization of the system (left) and of one particle (right). The real trajectory of one particle is drawn in the left image, with darker/lighter color indicating lower/higher speed, respectively. (b) Global translational kinetic energy ($T_t$) vs. upflow average speed ($u_{\text{air}}$), for $\phi = 0.25, 0.45$. Y axis is in log scale. As we can see, $T_t \equiv \langle T_t \rangle$, grows exponentially with $u_{\text{air}}$. Marginal distribution functions: (c) Of the particle speed ($v$), $f_{r,w}(v)$; (d) of the particle spin ($w$), $f_{r,v}(w)$. The spatial averages $\langle v \rangle_r, \Omega \equiv \langle w \rangle_r$ are indicated for each distribution ($f_{r,w}(v)$ and $f_{r,v}(w)$, respectively) with a vertical line with the same color as its distribution. Also, in panel (d), a black solid line is drawn with $w = 0$, in order to separate the reverse (counter clockwise, in this case) spin region ($w < 0$). Reduced 2D fields, for several $T_t$ values: (e-h) Reduced particle speed fluctuations $U^*(x,y) \equiv v_{\text{th}}(x,y)/V_0$, with $V_0 = \max(v_{\text{th}}(x,y))$: (e) $T_t = 0.66$; (f) $T_t = 0.35$; (g) $T_t = 1.48$; (h) $T_t = 2.54$. (i-l) Reduced average spin $\Omega^*(x,y) \equiv \langle w(x,y) \rangle/w_0$, with $w_0 = \max(\langle w(x,y) \rangle)$: (i) $T_t = 0.66$; (j) $T_t = 0.35$; (k) $T_t = 1.48$; (l) $T_t = 2.54$. In both $U^*(x,y)$ and $\Omega^*(x,y)$ color maps, brighter is higher and darker is lower; black stands for $U^*(x,y), \Omega^*(x,y) = 0$ and white for $U^*(x,y), \Omega^*(x,y) = 1$. $T_t \equiv \langle T_t \rangle_r$ is in units of $m_p \sigma^2/s^2$. In (e)-(l), the system boundary is marked with a thick yellow line. Area fraction for panels (c)-(l): $\phi = 0.25$. 

$\sigma = 72.5 \text{ mm}$
chirality with constant sign; the flow chirality reversal being observed as density increases [17]. However, we have surprisingly detected that the direction of flow circulation displays a complex behavior that is very sensitive to average kinetic energy of the particles. As we will see, we have additionally discovered that this complexity results from the balance between two distinct mechanisms, namely particle spin-velocity statistical correlations and heat dissipation at the outer walls.

For convenience, we use the notation \( \langle \ldots \rangle = \int n(r) \, \text{d}v \int \text{d}w \ldots f(r, v, w) \), where \( n(r) = \int \text{d}v \int \text{d}w f(r, v, w) \) is the particle density. We define also the global area fraction as \( \phi = N\sigma^2/L^2 \simeq N/100 \).

We define the field of translational kinetic energy fluctuations as \( T_t(r) = \langle (v \cdot w) \rangle \) (where \( v^2 = \langle v^2 \rangle = \langle (v - \langle v \rangle)^2 \rangle \)). It will also be useful to denote spatial averaging as \( \langle \ldots \rangle_r = \int \text{d}r \ldots \).

Figures 1(c), (d) show the marginal distribution functions,

\[
\begin{align*}
\mathfrak{f}_{r,v}(w) &= \langle \langle |v| - w \rangle \rangle_r, \\
\mathfrak{f}_{r,w}(v) &= \langle \langle w - |w| \rangle \rangle_r, \\
\end{align*}
\]

whose first moment averages increase for increasing air current (denoted as \( T_t \equiv T_t(r) \)). In [2], \( \delta(x = 0) = 1 \) and \( \delta(x \neq 0) = 0 \), and \( |v| = \langle (v_x^2 + v_y^2) \rangle^{1/2} \), and \( w = w_x \hat{e}_z \).

As we can see in Figures 1(c), (d), the shapes of the marginal distributions \( \mathfrak{f}_{r,v}(v) \), \( \mathfrak{f}_{r,w}(w) \) vary significantly versus airflow intensity. In particular, the marginal spin distribution (Figure 1(d)) displays an interesting behavior. At low activity levels (low upflow current intensity), the spin distribution extends to positive values (counter clockwise spin). This behavior is likely due to angular momentum transfer upon particle collisions [29], which can momentarily reverse particle spin. Arguably, the spin would rapidly return after collision to its clockwise rotation, as imposed by the blades orientation with respect to upflow. However, as upflow intensity increases, clockwise torque on particle blades becomes strong enough so as to neutralize the spin reversal mechanism upon particle collisions. Most notably, in the weak driving state, the marginal distribution displays a secondary maximum around \( w = 0 \). In spite of all this details in the collisional dynamics, we have consistently seen that the average particle spin is consistently negative in all experiments; i.e., we deal with a system for which the sign of the average particle chirality is constant, always negative (clockwise) in this case. Therefore, any possible structural changes in the steady states cannot be due to an eventual (non-existing) change in particle chirality. Figures 1(h), (i)-(l) the 2D density fields \( \nu_{r_h}(x, y) \equiv \sqrt{V^2} \) and \( \Omega(x, y) \equiv \langle w \rangle \), respectively. The (approximately) radial structure can be seen. It is also noticeable that particles do not occupy all the available space but concentrate in the central region. This kind of particle density behavior has not been observed at higher density (see the corresponding Figures 1(c)-1 for a higher packing fraction in the Supplementary Material [30]). Also, it is apparent that fluidization is weaker in the center for both particle velocity and spin, probably due to an enhanced cooling rate, due to more frequent particle-particle collisions [31].

We look up now at the fluid vorticity \( \omega \). The flow velocity \( u \) (stream lines) and vorticity (color map) are represented in Figures 2(a)-(c) for different (and increasing) upflow intensities. Each panel illustrates one of the three different vorticity behaviors we have found. It is apparent that the flow field has a broken symmetry, since its mirror image is not identical; i.e. the flows observed here have mirror chirality [28]. First, in panel (a), if the system is cold enough, fluid circulates in the same direction as the average particle spin (clockwise, in our system). We denote this behavior as spin wise chirality \( \mathbb{C}^+ \). Next, at intermediate activity levels (Figure 2(b), the system undergoes a transitional behavior with several vortexes, each with either spin wise or counter spin wise rotation. We denote this as complex chirality \( \mathbb{C} \pm \). Finally, for high driving (Figure 2(c), the system achieves complete chirality reversal, which we denote as counter spin wise chirality \( \mathbb{C}^- \). These transitions can also be seen in Movie 1 [30]. Figures 2(d), (e) analyze the behavior of the flow velocity and spin fields. In particular, for \( \mathbb{C}^+ \) states \( u(r) \) reaches its maximum at the midpoint between the center and system boundary, whereas for \( \mathbb{C}^+ \), \( \mathbb{C}^- \) the maximum is reached at the system boundary. On the other hand, the spin field \( \Omega(r) \) increases in magnitude for \( \mathbb{C}^+ \) remains essentially constant for \( \mathbb{C}^+ \) and \( \mathbb{C}^- \). In summary, both fields present a distinct behavior for each of the cases. This could indicate that the chirality mechanism is inherently different for the three chiral states \( \{ \mathbb{C}^+, \mathbb{C}^-, \mathbb{C}^- \} \).

Let us analyze in more detail the chirality transitions in Figure 3. As we can see in panel (a), the spatial averages of counter spin wise vorticity \( \omega^\mp = \langle \omega \Theta(\omega) \rangle \) and spin wise vorticity \( \omega^\pm = \langle \omega \Theta(-\omega) \rangle \) (here, \( \Theta(x) = 1 \) for \( x > 0 \) and \( \Theta(x) = 0 \) for \( x < 0 \) present inverse behaviors; i.e., spin wise vorticity monotonically decreases with \( T_t \) whereas counter spin wise vorticity increases monotonically. Due to this, \( \omega^\mp \) and \( \omega^\pm \) eventually cross at a given value of \( T_t \), that we identify as the critical point, and is slightly different for each density (see Figure 3(a) inset). These values (denoted as \( T_{c_t} \)) are shown in the inset. Partial vorticities have been reduced in Figure 3(a) with \( \omega^{\pm}_{\text{threshold}} \) and, as we can see, in this scaled representation the curves for different densities all collapse if \( T_t < T_{c_t} \) but split for \( T_t > T_{c_t} \), suggesting again that a different mechanism begins to govern the chirality behavior and that this mechanism is related to emergent boundary currents [3]. In effect, particle-wall collision frequency depends on the system density, which could account for this divergence.

The \( \mathbb{C}^+ \rightarrow \mathbb{C}^- \) transition clearly has a continuous nature (no abrupt transition from spin wise to counter spin wise vorticity is observed), because as we can see is
mediated by a distinct and continuously changing \( \mathbb{C} \pm \) phase, with several (instead of one) vortexes of both signs (Figure 2 (b), see also Movie 2 [30]). Nevertheless, one of the signs predominates in the \( \mathbb{C} \pm \), except at the critical point. Yet, identification of the \( \mathbb{C} \pm \) chirality is unambiguous as the count of vortexes in the system is higher than one. The transitions are graphically described in Figure 3 (b), which depicts the global vorticity \( \nabla = \nabla_+ + \nabla_- \) in the \( (\phi, T_r) \) parameter space.

Interestingly, it is not trivial that there should be a chiral transition as the one described here, nor that this transition should be necessarily continuous. For this reason, the results in Figures 2, 3 all lead us to consider that at least two different mechanisms compete in the phase behavior, balancing each other to different extents in the intermediate phase. Also, as we know, chirality emerges from an asymmetric part of the stress tensor [1] that is absent in regular fluids. One of the contributions to this asymmetric stress tensor is proportional to the odd viscosity [11]. This odd viscosity, as other transport coefficients, should emerge from the microscopic state structure of the system; i.e., the properties of the nonequilibrium velocity distribution function [31, 32].

On the other hand, it is evident, from Figures 2 (c), (d), that the distribution functions show in general significant deviations from the Maxwellian, which are more apparent for weak driving. These deviations off the Maxwellian have already been qualitatively described detected in previous works on chiral fluids (see for instance [17]). However, in order to provide a more precise and quantitative description, one has to resort to the properties of the cumulants of the distribution function, which additionally provide information on the statistical correlations present in the system [31]. Surprisingly, the distribution function cumulants and the statistical correlations they describe have so far remained unreported in the context of chiral flows. Thus, in order to investigate on the origin of the mechanisms producing the

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**FIG. 2.** (a)-(c) Stream lines and vorticity field for three experiments with the same area fraction \( \phi = 0.45 \) and \( T_r \equiv \langle T_r \rangle_r = \{0.63, 1.16, 2.65\} \) \( m_p(\sigma/s)^2 \) for (a), (b), (c), respectively. They represent the different chiral flow phases we have found: (a) chiral flow with rotation in the same direction as the particle spin, or spinwise, (we denote this phase as \( \mathbb{C}_+ \), clockwise in this case, and thus with negative vorticity \( \omega \)), (b) complex chiral flow (note the multiple vortexes with different sense of rotation, we denote this phase as \( \mathbb{C}_\pm \)), and (c) a system with counterclockwise fluid rotation, \( \mathbb{C}_- \). Panel (d) shows the radial profile of the flow velocity modulus \( u(r) \), each line corresponds to one of the experiments of the previous panels. (e) displays the mean particle angular velocity as we get away from the center. For spin-wise chirality (\( \mathbb{C}_+ \)), there is a clear gradient where particles move faster near the walls and slower in the central region; meanwhile, in complex or counter-clockwise situations particles maintain a steady self-rotation speed for every \( r \), this speed being larger in magnitude the stronger the driving.
so that they are null for an equilibrium Maxwellian distribution function \[ \langle \omega \rangle \] and quantifies velocity-spin correlations in the azimuthal direction (see Appendix A for more details). Notice that, according to its definition in (3), \( \epsilon_{00}^b > 0 \) when particles tend to orbit performing a rotation in the same sense as particles spin (i.e., the \( \mathbb{C}_+ \) phase), whereas for \( \epsilon_{00}^b < 0 \) the fluid would orbit in opposite sense to particle spin (the \( \mathbb{C}_- \) phase). Non chiral fluids or with chirality changing locally would display vanishing \( \epsilon_{00}^b \). In this way, we take into account the inherent anisotropy of the system. Also, \( \epsilon_{11}^0 \) measures correlations of the spin-velocities moduli. It is also relevant to consider the translational/rotational kinetic energy fluctuations ratio, \( T_0/T_1^r \), since this ratio indicates the degree of particle spin synchronization; i.e., when particles rotate at nearly the same rate (spins synchronize), \( T_0^r \) tends to be small against \( T_1 \) and thus \( T_1/T_0^r \) increases.

We plot in Figure 4 (a) the trends of the cumulants \( \epsilon_{11}^0 \) (blue symbols) and \( \epsilon_{00}^b \) (inset) reveal indeed that our system features correlations between rotations and translation. This coupling can yield the \( \mathbb{C}_+ \) chirality, as sketched in Figure 4 (c). In particular, it is interesting to note that the sign of the bend cumulant \( \epsilon_{00}^b \) evolves from negative for low \( T_1 \) to positive for high \( T_1 \), thus determining the changes of sign of the global vorticity \( \omega \). Also, the speed-spin correlations \( a_{11}^0 \) mostly vanish at higher \( T_1 \), when \( \mathbb{C}_- \) chirality is predominant, with a fast decreasing interval that roughly coincides with the transitional \( \mathbb{C} \pm \) chirality. This correlation decay is besides accompanied by a notable drop (of 2 orders of magnitude) of spin kinetic energy fluctuations relative to translational energy fluctuations (set of red points, right Y axis in Figure 4 (a)), as the system increases its activity (higher \( T_1 \)) and approaches the \( \mathbb{C}_- \) chiral state. This signals a process of spin synchronization that, apparently, allows for the decay of the \( \mathbb{C}_+ \) chiral mode. In summary, measurements indicate that correlations between rotation and translations at the level of the particle dynam-

\[
\begin{align*}
\epsilon_{11}^0 &= \frac{1}{2} \frac{(V^2)}{(V^2)^2} - 1, \\
\epsilon_{00}^b &= \frac{1}{2} \frac{(V^2)}{(V^2)^2} - 1, \\
\epsilon_{02}^b &= \frac{1}{2} \frac{(V^2)}{(V^2)^2} - 1, \\
\epsilon_{00}^b &= \frac{3}{2} \frac{(V^2)}{(V^2)^2} - 1.
\end{align*}
\]
 FIG. 4. (a) Particle velocity-spin correlations, vs. $T_t \equiv \langle T_t \rangle_r$, as measured from the cumulant $a_{11}^{(0)} = \frac{1}{3} \left( \frac{\langle V^2 \cdot W^2 \rangle - 1}{\langle V^2 \rangle \langle W^2 \rangle} \right)$ (blue series, left Y axis), and the ratio $T_t/\langle T_t \rangle_r$ (red series, right Y axis). Inset represents cumulant $a_{00}^{(0)}$ (dark grey color). The error bars of series of $a_{11}^{(0)}$, $T_t/\langle T_t \rangle_r$, and $a_{00}^{(0)}$ points are highlighted in blueish, reddish and grey backgrounds respectively. The transition interval in $T_t$, with complex chirality, is highlighted in yellow; a dashed line marks the chirality transition point $T_t$. Magnitudes are measured in different annuli of the system, each annulus marked with a different symbol: $\circ : 0.49 \sigma$, $\triangle : 1.47 \sigma$, $\square : 2.45 \sigma$, $\circ : 3.43 \sigma$ for $a_{11}^{(0)}$ and $T_t/\langle T_t \rangle_r$, and $\circ : 0.87 \sigma$, $\triangle : 2.62 \sigma$, $\circ : 4.36 \sigma$ for $a_{00}^{(0)}$; area fraction is $\phi = 0.25$. (b) Radial gradient $dT_t/dr$ (heat flux $q_t \propto (dT_t/dr)$), as a function of $T_t$, and measured at the boundary, i.e., $r \approx 5 \sigma$. Inset shows $dT_t/dr$ radial profiles for several values of $T_t$. (c) Interaction between two spinners result in rotation around their center of mass, this mechanism explains the transfer of intrinsic angular momentum into spin-wise circulation; this happens as long as spin and velocities are statistically correlated. (d) Particle-wall collisions result in a momentum transfer in the counter spin wise direction [3], the resulting edge flow propagation causes chirality reversal.

ics have distinctive features, according to the observed chiral phases.

The absence of correlations would not be the only factor involved in the build up of the C− mode. In fact, it is known that heat dissipation at the boundaries plays a significant role in flow chirality reversal as well [17]. In this sense, we observe that, in the C± mode, counter spin wise vortexes tend to become first predominant in the boundaries (see Figure 2 (b) and Movie 2 [30]), which could indicate that in effect the C− mode builds up from the boundaries. This effect has been already detected but not directly quantified yet. Thus, in Figure 4 (b), we plot $dT_t/dr$ vs. $T_t$ as measured at the boundaries (main panel) and vs. $r$ (inset), since the normal heat flux is proportional to $-dT_t/dr$ [32]. We find that the heat flux undergoes a significant increase for high $T_t$, coinciding with the emergence of the C± and, afterwards, the C− mode. The increase of heat dissipation at the boundaries indicates that wall-particle collisions (which are inelastic [31]) are more frequent. Due to a mechanism of tangential friction (roughness) on impact, this favors counter spin wise chirality after collision with the outer walls, see diagram in Figure 4 (d), and thus the subsequent flow chirality reversal.

However, it is important to remark that heat dissipation is also proportional to particle collision frequency [31], which notably drops at low densities. Therefore, the chirality reversal at low densities, as illustrated in Figure 3 (b) (for instance in the transitions found in the vertical lines at low densities) can only be explained by means of the spin synchronization mechanism that according to our observations is also strong at low densities (see low density series data in Figure 3). Moreover, we have found that the inversion occurs also for boundary-frictionless systems, as reported in Movie 3 [30] material, which reinforces the idea that transitions build up of changes in the statistical correlations and that boundaries are not necessarily involved in these processes (for more details on this question, see theoretical analysis in Appendix A).

IV. CONCLUSION

In summary, we have described a system of active spinners with a rich and non-trivial dynamical behavior, whose stationary flows feature three different chiral modes. The transition between these modes is controlled by the interplay of spin-velocity correlations and boundary heat dissipation, as we have shown; this in-
terplay being controlled by kinetic energy fluctuations (primary role) and particle density (secondary role). In particular, it is interesting to notice that the main chiral mode \( C^+ \) (for which fluid rotation is particle spin wise) is suppressed via a mechanism of spin synchronization and bend coefficient reversal, eventually enhanced by heat dissipation at the boundaries.

Let us remark here that the fact that changes in the details of the coupling between particle translations and rotations can induce changes in the average sign of particle chirality, which in turn induces a transition in the sense of rotation of the chiral flow has been already been studied in detail (see for instance \[13, 22–25\]). However, we report now a very different situation. That is, by studied in detail (see for instance \[13, 22–25\]). However, we report now a very different situation.

Therefore, we report here a strong experimental evidence that the sign of chiral flow is not necessarily determined by the type of particle chirality. In fact, it is statistical correlations between particle velocity and spin that directly determine the sense of rotation of the chiral flow. We think this result is also very relevant since, as a consequence, a variety of different chiral flows emerge now as accessible for constant chirality particles as well.

Furthermore, the transitions between the observed chiral modes are defect-mediated and continuous (due to the new and intermediate complex chiral phase \( C \pm \)), as opposed the transitions previously observed \[17\]. To be more precise and according to our results, flow chirality defects appear gradually (here, in the form of counter spinwise vortexes), thus yielding an intermediate and previously not reported complex chiral phase, which we denoted as \( C \pm \) (see Figure 2 a-c). This result is also relevant since it is in close analogy to the scenario of transitions in other systems, such as semiflexible filament bundles \[33\], or two-dimensional crystals \[34\]. Thus, clear links between chiral flow transitions and other systems emerge now, in a broader context in soft matter.

Finally, our results illustrate that the set of transport coefficients inherent to chiral fluids, including (but not only) odd viscosity \[4, 11\], would be controlled by the microscopic behavior (i.e., the non-equilibrium distribution function features) of the system, just in the same way as transport coefficients for regular fluids are \[33\]. Future development of a kinetic theory for this chiral of fluids would thus provide insight on their transport phenomena properties. We expect to fulfill this in future work.

Appendix A: Statistical mechanics of the two-dimensional chiral fluid

1. Properties of the kinetic equation

Let us now consider the global features that the kinetic equation should have for our system.

- First of all, particles display thermal-like translational movement (the concept of thermal-like movement for macroscopic particles was, probably, first introduced by Kanatani, see \[35\]). Thus, the kinetic equation should be provided with an external forcing term \( F^e \) that is acting stochastically each particle. This kind of forcing is usually denoted in non-equilibrium statistical mechanics as *stochastic thermostat* \[36\]. In this case we consider a stochastic thermostat in the form of a white noise \[37, 38\], which is defined by the relations \( \langle F_i(t) \rangle = 0 \), \( \langle F_i(t)F_j(t') \rangle = m^2 \xi_0 \delta_{ij} \delta(t-t') \), and \( \xi_0 \) is the forcing intensity. Notice that the forcing only correlates a particle with itself; i.e., there is no forcing between different particles (i.e., \( i \neq j \)).

- Secondly, let us point out that particle activity emerges within the rotational degrees of freedom. This activity is inherently chiral since it is rooted in the geometric configuration of the particle, which here has *chirality*. We will denote particles geometric chirality as \( C \), and rotational activity will be denoted as \( A(C|w) \).

- Lastly, particle collisions should also be chiral since momentum conservation laws imply, in general \[31\], a back and forth transfer between the translational and the (here, chiral) rotational degrees of freedom. Additionally, it cannot be expected that active particle encounters will involve some energy exchange \( \Delta E \) between the particles external dynamics and their internal degrees of motion. Therefore, collisions (encounters) between these active particles are *inelastic*; i.e., they will not preserve energy.

Therefore, and if we only consider the case of a low density fluid, so that particle encounters occur by pairs and their pre-collisional velocities are statistically uncorrelated; i.e., this implies a Boltzmann-like equation \[32\] with an inelastic \[39\] and chiral collision operator

\[
\frac{\partial f}{\partial t} + v \cdot \nabla f - \frac{\xi_0^2}{2} \frac{\partial^2 f}{\partial v^2} + A(C|w)[f] = J[r, v, (C|w); t|f, f]. \tag{A1}
\]

We have tagged with the symbol \( C \) each parity-violating term in Equation (A1). It is not the purpose of the present work to analyze a specific collisional model that, in the case of active particles can be rather involved \[40\]. However, for our purpose, it will suffice here to consider
for instance the feature of hard collisions. In this case, the two-particle collision operator \( J \) would be of the form

\[
J[r, v_1, (C|w_1); t|f, f] = \sigma \int dv_2 \int \mathcal{d}\mathbf{\sigma}(g \cdot \mathbf{\hat{\sigma}})(g \cdot \mathbf{\hat{\sigma}})
\times (b^{-1}\Delta E, C - 1) f(r, v_1, w_1, t) f(r, v_2, w_2, t),
\]

where here \( g = v_1 - v_2, \mathbf{\hat{\sigma}} \) is a unit vector along the line joining centers of the colliding particles (with velocities and spins \( v_1, w_1 \), respectively), and \( \Theta \) is the Heaviside function. The function \( b^{-1} \) operates on \( f \) in such a way that yields the particles velocities before the collision. Thus, it can be denoted as \textit{restituting} operator [39]. As we see, it is both chiral and inelastic, and this has a fundamental effect on the dynamics of the system.

Also, from Equation \( (A1) \) it is evident that there is a mathematically complex coupling between the chirality in the spin activity and chirality in the collision operator (which has a non-trivial integro-differential form), and as a result, it cannot be asserted that chirality of the flow field \( u \) will yield a flow vorticity whose chirality sign will necessarily coincide with that of \( (C|w) \) (vorticity is defined here as \( \omega(r) = (1/2)e_{ij}\partial_i u_j, \) where \( e_{ij} \) is the 2D Levi-Civita symbol).

The question of the emergence of a fluid vorticity from a chiral flow pattern and the direction of this vorticity is the fundamental question in the field of chiral active matter (see for instance the last paragraph of section B2, page 16 in [41]; or also references [3] [42] for instance, and most of the other ones in the bibliography) and the analysis above vows to illustrate the fact that this question is not trivial and cannot depend on the sign of particle chirality/activity or boundary conditions alone. Rather, it is a combination of those together with the collisional properties of particle-particle collisions which will determine: a) if chiral particles will produce a chiral flow at all; and b) if the flow chirality has the same or opposite sign as particle chirality.

Furthermore, chirality of the system should emerge in the particle distribution itself, as we have explained. Therefore, the distribution function should contain variables that are able to express this parity violations taking place in the system. We analyze this in the next subsection.

2. Particle velocities distribution function

We will consider in this work stationary states only (distribution functions are time-independent), thus, \( \partial / \partial t = 0 \) in \( (A1) \). Additionally, if we consider small spatial gradients, a normal solution for \( f \) [39] should be attainable, i.e., all of the space dependence of the distribution function can be expressed through the relevant fields [39]. In this case, this implies \( f(r, v, (C|w)) = f(n, (C|u(r)), (C|\Omega(r))(r)) \), which shows that chirality will be transmitted from particle to average fields level, and thus the chiral flow observed in Figure 1.

Moreover:

- The distribution function \( f(r, v, w) \) will inherently have also chirality. Thus, a plausible way to describe is them through a vectorial coupling of \( v \) and \( w \). For instance, the magnitude \( \cos \alpha \equiv (v \times w) \cdot \mathbf{\hat{e}}_\phi / |v \times w| \) would feature these properties.

- \( f(r, v, w) \) should be sensitive to the sign of \( \cos \alpha \); since for \( \cos \alpha < 0 \) the particle spin-velocity correlation is clockwise, thus favoring clockwise particle circulation, and thus clockwise flow vorticity. Conversely, for \( \cos \alpha > 0 \), counter clockwise flow vorticity is favored. In this way, we guarantee that \( f \) has the ability to display different flow vorticity behaviors for the same particle chirality \( (C|w) \).

We define the relevant average fields, particle density \( n \), fluid flow \( \mathbf{u} \) and average particle spin \( \mathbf{\Omega} \)

\[
n(r) = \int dv \int dw f(r, v, w),
\]

\[
\mathbf{u}(r) = (1/n(r)) \int dv \int dw f(r, v, w) \mathbf{v},
\]

\[
\mathbf{\Omega}(r) = (1/n(r)) \int dv \int dw f(r, v, w) \mathbf{w},
\]

and \( T_t \) (translational kinetic energy fluctuations) and \( T_r \) (rotational kinetic energy)

\[
T_t(r) = \frac{m_p}{2n(r)} \int dv \int dw f(r, v, w)(\mathbf{v} - \mathbf{u}(r))^2,
\]

\[
T_r(r) = \frac{I}{2n(r)} \int dv \int dw f(r, v, w)w^2,
\]

with \( w = w_z \) (in our 2D system) and \( m_p, I \) are particle mass and moment of inertia, respectively. We also define the spin kinetic energy fluctuations

\[
T_r^*(r) = \frac{I}{2n(r)} \int dv \int dw f(r, v, w)(\mathbf{w} - \mathbf{\Omega})^2.
\]

The scale of \( T_t \) and \( T_r^* \) in our system will in general be different.

For convenience, we define \( \mathbf{V} \equiv \mathbf{v} - \mathbf{u}(r), \mathbf{W} \equiv \mathbf{w} - \mathbf{\Omega}(r); V = (\mathbf{V} \cdot \mathbf{V})^{1/2}, \quad W = (\mathbf{W} \cdot \mathbf{W})^{1/2} \). Let us also define the bivariate Maxwellian

\[
f_{2M}(r, V^*, W^*) =
\]

\[
n(r) \left( \frac{m_p}{2\pi T_t(r)} \right)^{1/2} e^{-\frac{V^2}{2T_t(r)}} e^{-\frac{W^2}{2T_r^*(r)}}
\]

\[
\equiv n(r) \left( \frac{m_p}{2\pi T_t(r)} \right)^{1/2} e^{-V^{*2}} e^{-W^{*2}}.
\]

Henceforth, we use the notation:

\[
V^* = V/(2T_t/m_p)^{1/2} \equiv V/\langle V \rangle^{1/2},
\]

\[
W^* = W/(2T_r^*/I)^{1/2} \equiv W/\langle W^2 \rangle^{1/2}
\]
for j-th powers of translational velocities and angular velocities, respectively, where we have taken into account

\[ f(r, V^*, W^*, \cos \alpha) = \]

\[ f_{2M}(r, V^*, W^*) = \sum_{j,k,\ell=0}^{\infty} a_{jk}^{(\ell)} L_{j}^{(\ell+\ell_0)}(V^{*2}) L_{k}^{(\ell+\ell'_0)}(W^{*2}) P_{\ell}(\cos \alpha) W(V^{*2}, W^{*2}, \cos \alpha) \]

\[ = n(r) \frac{m}{2T_r(r)} \left( \frac{I}{2T_r^2(r)} \right)^{1/2} \sum_{j,k,\ell=0}^{\infty} a_{jk}^{(\ell)} L_{j}^{(\ell+\ell_0)}(V^{*2}) L_{k}^{(\ell+\ell'_0)}(W^{*2}) P_{\ell}(\cos \alpha) (\pi^{-3/2} e^{-V^{*2}} e^{-W^{*2}}) W(V^{*}, W^{*}, \cos \alpha), \]

where \( j, k, \ell \) are positive integers and \( \ell_0, \ell'_0 \) are (integer) constants. Symbols \( L_{j}(x) \), with \( \ell \) being an integer, stand for the associated Laguerre polynomials of order \( (j, \ell) \), and with \( x \in [0, \infty] \). They are also commonly denoted, in the context of kinetic theory, as Sonine polynomials \([44, 45]\). Also, \( P_{\ell} \) are the Legendre polynomials.

The independent variable \( \cos \alpha \) characterizes particle chirality, and is defined here as

\[ \cos \alpha \equiv \frac{v \times w}{|v \times w|} \cdot \hat{e}_z = \frac{v_y e_y - v_z e_z}{|v \times w|} \cdot \hat{e}_z = \frac{-y e_y + x e_z}{r} = -sgn(w_z) \frac{v \cdot r}{v} \cdot \hat{e}_z = -sgn(w_z) \frac{v \times r}{v}. \]

Notice, from \([A7]\), that determination of \( \cos \alpha \) involves also knowledge of particle position and thus, it will be considered henceforth as an integration variable that is independent of reduced particle velocity \( (V^*) \) and spin \( (W^*) \). Also, notice that these three formulas combined imply that in our system \( \cos \alpha < 0 \) is to be expected for a flow whose vorticity is counter clockwise, and hence flow rotation has the same as particles spin. We will denote this situation as \( \mathbb{C}_+ \) (or spinwise, SW) chiral flow phase. Conversely, for \( \cos \alpha > 0 \) yields clockwise vorticity; i.e.,

We can write the distribution function as a polynomial expansion around \( f_{2M}(r, V^*, W^*) \).

\[ \text{vorticity is counter spinwise (CSW), which we denote as } \mathbb{C}_-. \]

The product of associated Laguerre and Legendre polynomials both configure the set of orthogonal polynomials \( L_{j}^{(\ell)}(V^{*2}) L_{k}^{(\ell)}(W^{*2})(V^{*}W^{*})^{2\ell} P_{\ell}(\cos \alpha) \) in \([A2]\). Use of the shifted Legendre polynomials \([41, 46]\) is not justified here since, as we said, particle chirality depends on the sign of \( \cos \alpha \). The weight function \( W(V^*, W^*, \cos \alpha) \) is determined so that

\[ \int dV^* \int dW^* \int d(\cos \alpha) W(V^*, W^*, \cos \alpha) \]

\[ = \int dV^* \int dW^* \int d(\cos \alpha) w_{l}(V^{*2}) w_{l}(W^{*2}) w_{p}(cos \alpha) \]

where \( w_{l}(x) \equiv e^{-x} x^{\ell} \) and \( w_{p}(x) \equiv 1 \) are the weight functions of the associated Laguerre and Legendre polynomials respectively \([46]\). Taking into account that \( (m_r/2T_r(r)) \int dV^* = 2 \pi \int V^* dV^* = \pi^{3/2} e^{-V^{*2}} e^{-W^{*2}} W^{*2} \), we obtain

\[ W(V^*, W^*, \cos \alpha) = \pi^{3/2} W^* (V^{*}W^{*})^{2\ell}. \]

Therefore, for products of the type \( L_{j}^{(\ell+\ell_0)}(V^{*2}) L_{k}^{(\ell+\ell'_0)}(W^{*2}) P_{\ell}(\cos \alpha) \) \( f(r, V^*, W^*, \cos \alpha) \), we obtain

\[ \int dV \int dW \int d(\cos \alpha) \left[ L_{j}^{(\ell+\ell_0)}(V^{*2}) L_{k}^{(\ell+\ell'_0)}(W^{*2}) P_{\ell}(\cos \alpha) \right] f(r, V^*, W^*, \cos \alpha) \]

\[ = n(r) \sum_{j,k,\ell=0}^{\infty} \int_{0}^{\infty} dV^{*2} \int_{0}^{\infty} dW^{*2} \int_{-1}^{+1} d(\cos \alpha) \left( L_{j}^{(\ell)}(V^{*2}) L_{k}^{(\ell)}(W^{*2}) P_{\ell}(\cos \alpha) \right) \left( L_{j}^{(\ell)}(V^{*2}) L_{k}^{(\ell)}(W^{*2}) P_{\ell}(\cos \alpha) \right) \times e^{-V^{*2} - W^{*2}} (V^{*}W^{*})^{2\ell} \]

\[ = n(r) \sum_{j,k,\ell=0}^{\infty} a_{jk}^{(\ell)} \frac{\Gamma(j + \ell + 1) \Gamma(k + \ell + 1) 2^{j} \delta_{j,k} \delta_{\ell,\ell'}}{j! k! 2\ell + 1} = n(r) a_{jk}^{(\ell)} \frac{\Gamma(j + \ell + \ell_0 + 1) \Gamma(k + \ell + \ell'_0 + 1) 2^{2\ell + 1}}{j! k! 2\ell + 1}, \]
Thus, by replacing \( x \to L \) guerre polynomials are the thermodynamic equilibrium state.

The integral in (A 2), for \( j = 1, k = 0, \ell = 0 \), taking into account also (A 4)

\[
\int dV \int dW \int d(cos \alpha) L_1^{(0)}(V^{*2}) L_0^{(0)}(W^{*2}) P_0(cos \alpha) f(r, v, w) = \int dV \int dW \int d(cos \alpha)(1 + \ell_0 - V^{*2}) f(r, v, w)
\]

The integral in (A 2), for \( j = 0 \) and \( k = 0 \), we determine the constants \( \ell_0 \), \( \ell_0' \) and \( a_{00}^{(1)} \).

The next step is to determine the constants \( \ell_0 \), \( \ell_0' \) and \( a_{00}^{(1)} \).

In order to determine the constants \( \ell_0 \), \( \ell_0' \) we determine the integral in (A 2), for \( j = 1 \), \( k = 0 \), \( \ell = 0 \), taking into account also (A 4)

\[
a_{20}^{(0)}(r) = \frac{1}{2} \left( \frac{1}{2} \langle V^4 \rangle - 1 \right),
\]

\[
a_{02}^{(0)}(r) = \frac{1}{2} \left( \frac{1}{2} \langle W^4 \rangle - 1 \right),
\]

\[
a_{11}^{(0)}(r) = \frac{1}{2} \left( \frac{\langle V^2 W^2 \rangle}{\langle V^2 \rangle \langle W^2 \rangle} - 1 \right),
\]

\[
a_{00}^{(1)}(r) = \frac{3}{2} \frac{\langle v \times w \rangle}{\langle v \times w \rangle},
\]

where for the expression of \( a_{00}^{(1)} \) we have taken into account the definition \( \cos \alpha \equiv (\langle v \times w \rangle \cdot \hat{e}_\phi)/|\langle v \times w \rangle| \).

The cumulant \( a_{00}^{(1)} \) characterizes particle translation-spin correlations. However, notice that for characterization of particle translation-spin correlations we use instead the slightly different coefficient \( a_{00}^{(b)} \)

\[
a_{00}^{(b)} = \frac{3}{2} \langle v^* \times w^* \rangle \cdot \hat{e}_\phi,
\]

(with \( v^* \equiv v/\sqrt{\langle v^2 \rangle} \) and \( w^* \equiv w/\sqrt{\langle w^2 \rangle} \) which retains analogous statistical information on the relative orientation of particle translations and spin, while holding a closer analogy to the bend coefficient used in elasticity theory [28]. For this reason, we used \( a_{00}^{(b)} \) to characterize translation-spin correlations in Figure 4 (a) in the main file.

Appendix B: Materials and experimental methods

We describe in this section the experimental methods. Additional experimental results and data, together with a description of experiments movies are provided in the Supplementary Material file and in an external data set [30].

The particles we used in our experiments are 3D-printed polylactic acid (PLA) disks of diameter \( \sigma = \ldots \)
72.5 mm and height $h = 6$ mm and they have 14 oblique blades that generate a clock-wise spinning as an air flow passes through the disk (see Figure 1(a)). The rotors are located on top of a perforated steel sheet (3 mm diameter holes in a hexagonal pattern, with a 3 mm spacing), this grid has been carefully leveled and is mounted on a box that guides an adjustable air current, generated by a fan and homogenized by means of a polyurethane foam layer; uniformity of the airflow is verified with an anemometer and local deviations are found to be within $\pm 5\%$ of the averaged value; mean air flows ranged from 2.2 to 3.2 m/s. Our disks are contained inside a circular PLA border of 725 mm diameter.

We have recorded a total of 120 experiments, carefully varying the parameters (density and air current), each realization consists of two movies (filmed with a Phantom VEO 410L high-speed camera). The first has a duration of 27.75 s and is recorded at 900 frames per second, which allows for measuring particles spin. The second take has a duration of $\sim 100$ s at 250 fps, and is used to calculate vorticity and the other relevant fields. Positions are calculated using a modified version of Crocker and Grier algorithm [47], obtaining a spatial resolution of around 0.05 % of the particle diameter. Meanwhile, spinner angular velocities were found using a custom method based on tracking blade luminosity, the accuracy in the measurement of frame-to-frame angular displacements is $\pm 3.5 \times 10^{-3}$ rad.

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SUPPLEMENTARY FIGURES AND EXPERIMENTS MOVIES

In this work we have recorded a total of 120 movies, covering a wide range of densities, going from $\phi = 0.03$ to $\phi = 0.70$. We could not represent this comprehensive experimental database. We include here, however two additional figures, 3 supplementary movies and experimental data.

- **Additional Figures:** The first supplementary figure is analogous to Figure 1 in the main text, except that here the packing fraction is $\phi = 0.55$. Figure 5 in this Supplementary Material one can see that the bimodal behavior of the spin distribution function is stronger than in the lower density case (shown in the main text). Also, from panels c-j we now see that particle cover the entire area of the system. The second supplementary figure (Figure 6) includes data for the cumulants defined in Eq. 2 (main text) that are not represented by Figure 4 in main text.

- **Supplementary Movies 1 & 2:** We included two additional movies in order to help the reader understand the most relevant results. In Movie 1, we show three configurations with constant density but an increasing thermalization level ($T_0 = \{0.63, 1.16, 2.65\} m_p(\sigma/s)^2$), this movie illustrate the chirality reversal caused by interaction with the system boundaries, we display the trajectories of three representative particles for each case. Movie 2 displays the evolution of the vorticity field for a sample experiment, there we show a situation of complex chirality with several vortexes of opposite directions, these vortexes evolve with time.

- **Supplementary Movie 3:** Experiment movie for $N = 3$. It can be seen by eye that the chiral flow inversion occurs without intervention of the boundaries. Hence, chiral flow inversion is not in general boundary-driven.

DATA AVAILABILITY

The data that support the plots within this paper and other findings of this study are available in the following web link: https://zenodo.org/record/4756796.

CODES AVAILABILITY

The particle tracking codes that were used for this work are available in the following web link: https://github.com/fvegar/blades.
FIG. 5. (a) Translational particle velocity distributions \( v \), \( f_{v,\nu}(v) \) for a system with \( \phi = 0.55 \) and four different values of \( T_t \), (b) particle spin distribution \( w \), \( f_{v,\nu}(w) \). In (a)-(b), dashed vertical lines indicate the mean of each distribution function (follow color correspondence). In (b), the continuous vertical line indicates separation between \( \omega < 0 \) and \( \omega > 0 \). (c-f) Reduced particle speed fluctuations \( U^*(x, y) \equiv v_{th}(x, y)/V_0 \). (g-j) Reduced average spin \( \Omega^*(x, y) \equiv \langle w(x, y) \rangle/w_0 \). In both \( U^*(x, y) \) and \( \Omega^*(x, y) \) color maps, brighter is higher and darker is lower; and black stands for \( U^*(x, y), \Omega^*(x, y) = 0 \) and white for \( U^*(x, y), \Omega^*(x, y) = 1 \). \( T_t \) is in units of \( m_p\sigma^2/s^2 \). The system boundary is marked with a thick yellow line.

FIG. 6. In this figure we plot, vs. \( T_t \), the cumulants \( a_{20}^{(0)} \) (blue, Y axis at the left), \( a_{02}^{(0)} \) (red, Y axis at the right in logarithmic scale). Each point represents the value for a single experiment. We show that the systems are clearly not Maxwellian (values far from zero). Also, there is no clear trend of either \( a_{20}^{(0)} \) nor \( a_{02}^{(0)} \) as a function of \( T_t \).