Article

Thermally Induced Mechanical Stress in the Stator Windings of Electrical Machines

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Abstract: The lifetime of an electrical machine mainly depends on the thermal overloading. Modern day applications of electrical machines on one hand require compact machines with high power density, while on the other hand force electrical machines to undergo frequent temperature cycling. Until recently, in the case of electrical machines, the main factor related to the degradation of the winding insulation was thought to be the thermal oxidization of the insulation materials. It has now been revealed that thermal overloading can also induce mechanical stress in the windings of electrical machines, which over time could lead to fatigue and degradation. In this paper, a comprehensive study of the thermally induced mechanical stress in the windings of an electrical machine is presented. The study is performed using combined thermo-mechanical models. The numerical results are validated by experiments on a segmented stator winding set-up.

Keywords: electrical machines; mechanical stress; stress; switched reluctance machines; temperature; thermal analysis

1. Introduction

Several modern day applications cause the temperature in the drive-train to vary continuously. In industrial drive-trains, for example, in weaving looms, the variation can be cyclic. But in applications such as electric vehicle drive-trains, the temperature variation can be non-cyclic. Nevertheless, the temperature variation in the drive-trains has significant effects on all its components, especially the power electronics and the electric motors [1]. The typical failures of electrical motors associated with the thermal cycling are the failure of the stator winding insulation [2–4] and the demagnetization of the permanent magnets [5].

One main source of heat in an electrical machine is the power loss in the stator winding. Improper heat removal leads to reduced lifetime of the windings [6] and thus the machine, due to the degradation of copper wires and the coatings which is caused by rapid oxidization of the coatings [7]. For better heat transfer and removal, the windings in electrical machines are subjected to epoxy impregnation, which on one hand ensures improved heat removal and on the other hand prevents the coatings from being in direct contact with air, thus preventing oxidization of the coatings. However, the difference in the coefficient of thermal expansion between the epoxy, coating and the copper wires might lead to thermally induced mechanical stresses in the windings which subsequently cause degradation of the windings.

2. Thermally Induced Mechanical Stress

Thermally induced mechanical stress itself is not a new subject of study. Several studies reporting the mechanical stress of thermal origin can be found. The deformation in solder joints resulting
from the stress caused by the thermal expansion mismatch is presented in Reference [8]. According to Reference [9], the mismatch of the thermal expansion coefficient can induce mechanical stress in electronic assemblies not only by the temperature cycling during normal operation, but also due to the high temperatures experienced during fabrication, shipping and storage. The failure of copper through silicon vias due to the thermally induced mechanical stress has been presented in References [10,11]. Mechanical deformations in electric interconnects due to thermal expansion mismatch has been reported in References [12,13]. The effects of the thermally induced mechanical stresses on light emitting diodes, plastic ball grid arrays and field-programmable gate arrays are studied and discussed in References [14–16].

Similar studies on the effect of thermally induced stress on different composite and cement-based materials have also been reported in literature. In Reference [17], the authors analyzed thermal stresses in two phase composites both numerically and analytically. The modeling of the degradation and failures of IGBT modules considering the electrical, thermal and mechanical stresses has been studied in Reference [18–20]. It has been found that the bond wire/substrate interface is the most vulnerable as it is affected the most by the thermally induced mechanical stress.

Although the thermally induced mechanical stress has been widely studied for electronics packages, power electronics and other fields, very little work was found for an electric motor. The development of shear stresses between winding components due to thermal cycling has been listed as one of the ageing mechanisms of the stationary armature winding in electrical machines in IEEE Standard-56 (2016) [21]. Nevertheless, very few publications dealing with research on the topic were found. One reason could be that such stress would be insignificant if the windings of the machine are not epoxy impregnated, because the coefficients of thermal expansion of copper and coating are similar. However, modern compact machines have epoxy impregnated windings for improved heat removal, as shown in Figure 1. Epoxy typically has a very high coefficient of thermal expansion. This can lead to significant stress, making a detailed study necessary.

A possible failure due to different expansion ratios of the core and the windings in large electric machines was first briefly reported by J. Wood in 1995 [22]. The difference in the thermal expansion coefficients of the copper and the ground wall insulation has been reported as a cause to yield a tensile stress [23]. According to Reference [24], rapid thermal cycling with the winding temperature possibly greater than 120 °C could lead to the fatigue crack between the copper and the insulation or within the insulation layers. This could eventually cause the partial discharge to occur. Although some reports on effects of mismatch of thermal expansion coefficients were found, the actual study on the thermally induced mechanical stress in the windings of an epoxy impregnated traction motors was not published until recently [25,26]. In Reference [25], author Z. Huang derives an analytical expression for the thermally induced mechanical stress and numerically calculates the stress in a single copper wire with
polymer coating surrounded by epoxy. The stress in a 4x4 multiple wire system simulated for even and uneven temperature distributions has been presented in Reference [26].

According to Reference [25], in an object with uniform temperature distribution, a change of temperature will cause a uniform thermal strain on the object, which can be expressed as

\[ \epsilon_{th} = \alpha (\Delta T) \]  

Here, \( \alpha \) is the coefficient of thermal expansion and \( \Delta T \) is the change in temperature. Based on (1), the analytical expression for the thermally induced mechanical stress in an object with two bonded materials has been derived. For instance, if two materials X and Y are bonded, the thermally induced mechanical stress experienced by each material is given by

\[ \sigma_X = \frac{(a_X - a_Y) \Delta T E_X E_Y A_Y}{E_X A_X + E_Y A_Y} \]  

\[ \sigma_Y = \frac{(a_Y - a_X) \Delta T E_Y E_X A_X}{E_X A_X + E_Y A_Y} \]  

where, \( E \) and \( A \) are the Young’s Modulus and the cross-sectional area of the materials, respectively.

The main focus of the study in References [25,26] is to justify that the lifetime degradation of the windings in a traction motor is not just the result of thermal oxidization. It is to justify that the thermally induced mechanical stress should also be taken into consideration. In both papers, the authors present numerically computed stress in the polymer coating and epoxy, but no experimental validation of the numerically computed stress has been shown.

In this paper, a comprehensive study of the thermally induced mechanical stress on the stator windings of an electrical machine is presented. A stator slot with windings generally consists of copper wires together with coating, epoxy (if impregnated) and insulations. When designing an electrical machine, a higher copper fill factor is desired. Compressed copper wires with a high fill factor reduces the dc winding losses and provides better heat transfer [27]. Since the copper fill factor not only affects the phase resistance and the current density but also the slot heat density, it is also an important parameter from the thermal design perspective. In addition, different epoxy resins with different coefficients of thermal expansion are available in the market. Therefore, to make the study more general, parametric studies are done by varying parameters like the copper fill factor, coefficient of thermal expansion of the epoxy and temperature. The numerically calculated stress is validated by experiments on a set-up identical to that used in the numerical simulation.

3. Numerical Model

The thermally induced mechanical stress in the stator windings of an electrical machines is investigated numerically using the Comsol Multiphysics software. Three-dimensional thermo-structural simulations are performed for this purpose. A stator of a 6-pole switched reluctance machine is used as a test case in the study, the 2D cross-section of which is shown in Figure 2. The most relevant geometrical dimensions of the machine are listed in Table 1.

Modeling electrical machines in 3D is itself a cumbersome task. The problem becomes more complex if all wires in the winding are to be included in the model. Therefore, to simplify the task, the geometry in this study is subjected to some simplifications which are as follows: (1) only a segment of the stator is modeled, (2) only half of the effective axial length of the machine is used in the simulations, (3) the number of turns of copper wires is reduced to 39 and (4) the enamel coatings of the copper wires are not included in the model. The geometry used in the study is shown in Figure 2. Notice that the winding has a rectangular cross section, and does not follow the curvature of the stator yoke, as is shown in Figure 2b. The reason is that in the experimental setup (Section 6), the winding is made as a form coil with rectangular cross-section, as is common practice for machines with concentrated windings.
The finite element mesh consists of 2,286,687 tetrahedral elements. The boundary conditions used in the simulation are more clearly illustrated figuratively in Figure 2. The boundary conditions used in the structural model are very important for accurate computation of the stress. A symmetric boundary condition has been used on adjacent sides in the circumferential direction. Since only half of the axial length is used in the simulations, the back face of the geometry has also been modeled with a symmetric boundary, while the front face is free to move. In addition, the upper and lower face along the radial direction are also modeled as free to move. The magnetic material grade is N020. The epoxy resin used is Epoxylite TSA 220 (Elantas Europe GmbH, Hamburg, Germany). Type M, enameled copper wire with temperature index of 210 has been considered. Table 2 lists the relevant material properties of the materials used in the simulations and experiments.

Figure 2. (a) 2D cross-section of an SR machine and (b) section of the stator with windings considered for the 3D model together with the boundary conditions used in the structural simulations.

Table 1. Geometrical dimensions of the machine.

| Parameters                               | Value     |
|------------------------------------------|-----------|
| Number of stator poles                   | 6         |
| Outer diameter of stator (mm)            | 120       |
| Inner diameter of stator yoke (mm)       | 98        |
| Thickness of the tooth (mm)              | 17.5      |
| Stack length (mm)                        | 80        |
| Number of turns per coil                 | 39        |

The magnetic material grade is N020. The epoxy resin used is Epoxylite TSA 220 (Elantas Europe GmbH, Hamburg, Germany). Type M, enameled copper wire with temperature index of 210 has been considered. Table 2 lists the relevant material properties of the materials used in the simulations and experiments.

Table 2. Thermal and mechanical properties of the materials.

| Properties                        | Electrical Sheet (N020) | Copper | Epoxylite TSA 220 |
|-----------------------------------|------------------------|--------|-------------------|
| Young’s Modulus (Pa)              | $200 \times 10^9$      | $1.1 \times 10^{11}$ | $3.5 \times 10^9$ |
| Poisson’s Ratio                   | 0.29                   | 0.35   | 0.34              |
| Thermal Conductivity (W/m·K)      | 28                     | 400    | 0.21              |
| Density (Kg/m³)                   | 7650                   | 8960   | 1180              |
| Heat capacity at constant pressure (J/Kg·K) | 440                 | 385    | 400               |
| Coefficient of Thermal Expansion (1/K) | $12 \times 10^{-6}$  | $18 \times 10^{-6}$ | $50 \times 10^{-6}$ |

The model used in the study can be considered as a combined thermo-structural model. It is considered combined in a sense that first, a temperature distribution over the entire volume is calculated by solving a thermal model; then, the computed temperature is used as an input in the structural model.

The boundary conditions used in the structural model are very important for accurate computation of the stress. A symmetric boundary condition has been used on adjacent sides in the circumferential direction. Since only half of the axial length is used in the simulations, the back face of the geometry has also been modeled with a symmetric boundary, while the front face is free to move. In addition, the upper and lower face along the radial direction are also modeled as free to move. The boundary conditions used in the simulation are more clearly illustrated figuratively in Figure 2. The finite element mesh consists of 2,286,687 tetrahedral elements.
The mechanical stress in the stator core, copper wires and epoxies are determined for two different cases: Case I: Uniform temperature distribution and Case II: Non-uniform temperature distribution. The results and discussion for both the cases are presented in the following sections. The stress is shown as the von-Mises stress, which is calculated as

$$\sigma_{\text{von-mises}} = \sqrt{\frac{1}{2} \left( (\sigma_{11} - \sigma_{22})^2 + (\sigma_{22} - \sigma_{33})^2 + (\sigma_{33} - \sigma_{11})^2 \right)} + 6 (\sigma_{12}^2 + \sigma_{23}^2 + \sigma_{31}^2)$$

(3)

where $\sigma_{11}$, $\sigma_{22}$, and $\sigma_{11}$ are the tensile stress coefficients which act along the axes and $\sigma_{12}$, $\sigma_{23}$, and $\sigma_{11}$ represent the shear stress which act along the planes.

4. Uniform Temperature Distribution

In this case, the temperature throughout the volume is considered to be uniformly distributed. The mechanical stress induced in the stator winding segment is calculated for a uniform temperature distribution of 150 °C. The von-Mises stress distribution over the entire volume is shown in Figure 3. The stress is relatively higher in the regions close to the interface of two materials. This is due to the difference in the coefficient of thermal expansion of the materials. For instance, in Figure 3, the areas of the stator tooth close to the windings have high stress, due to the difference in the coefficient of thermal expansion of the iron and epoxy in the windings. The stress is more concentrated towards the bottom corner of the tooth and the copper wire in the vicinity because of the deformation caused by the expansion.

![Figure 3](image)

**Figure 3.** The von-Mises stress distribution over the entire volume. Higher stress is seen near iron-epoxy interface, especially in the corner and tooth tip.

The stress in the copper wires together with the epoxy is shown in Figure 4. The wires on the outer layer are seen to have relatively higher stress compared to the ones in the middle layers. This is probably because the copper wires in the middle are symmetrically surrounded by the epoxy. Therefore, the expansion caused by heating is symmetrically distributed around the wires in the middle layers. However, in the inner layer and the outer layer, the expansion is not symmetric because the inner layer is close to the tooth and the outer layer is exposed to a large volume of epoxy.
This can also be noticed in Figure 5, which shows the stress distribution in the epoxy at different axial positions. In Figure 5, the stresses in the epoxy around the copper wires of inner and outer layers are relatively higher than those in the epoxy around the middle layer wires. Moreover, the stress on the upper half of the epoxy is higher on the front face, while on the lower half, the stress is seen to increase along the axial length. This is also related to the boundary conditions, as the front face and the top boundary are modeled as free to move boundaries causing lower stress due to the deformation, while the back face has a fixed boundary condition which leads to high stress.

The main aim of this study is to investigate the stress on the windings. Therefore, it is important to note the magnitude of the stress on the windings, which consists of the copper wires and the epoxy. From Figure 4, it can be seen that the winding can undergo a stress up to 197 MPa. This is a quite high value especially if we consider the coatings of the copper wire. Usually, copper wires are coated with polymers like Polyamide-imide, the tensile strength of which is about 250 MPa. The thermal expansion coefficient of Polyamide-imide is around the same value as copper. Therefore, the coating would undergo similar stress as the copper wires. Few cycles of such high stress could easily lead to the failure of the wire insulation. Although 197 MPa is the maximum stress that could occur in the winding, not all the wires are exposed to such stress. The average of the stresses in all the wires is about 44 MPa.

On the epoxy alone, the stress can reach as much up to 69 MPa, as seen in Figure 5. This magnitude is much lower than the stress in the iron and copper seen in Figures 3 and 4. Nevertheless, it is still significant when compared to the tensile strength of the epoxy. Consequently, it could also lead to fatigue and breakdown of the epoxy. It can be understood from these results that high temperatures
in the machine is responsible not only for the breakdown of the wire insulation due to oxidization, but also induces mechanical stress that could lead to the degradation of the insulation and the epoxy ultimately leading to the failure of the winding.

To get more assessment of the thermally induced mechanical stress, additional parametric studies were done. The parameters are the copper fill factor and the coefficient of thermal expansion of the epoxy ($a_{\text{epoxy}}$). A uniform temperature of 150 °C was used in the simulations. In the results shown in Figures 3–5, the copper fill factor was 0.6 and the thermal expansion coefficient of the epoxy was $50 \times 10^{-6}$ (1/K). The parameter values used in the parametric studies are listed in Table 3. The maximum stress on the copper wire in the middle of the winding and the epoxy is plotted as a function of the copper fill factor and $a_{\text{epoxy}}$ in Figures 6 and 7, respectively.

### Table 3. Value of the parameters used in the parametric studies.

| Parameter          | Value       |
|--------------------|-------------|
| Copper fill factor | 0.32 0.4 0.5 0.6 |
| $a_{\text{epoxy}}$ (1/K) | $25 \times 10^{-6}$ $50 \times 10^{-6}$ $75 \times 10^{-6}$ $100 \times 10^{-6}$ |

**Figure 6.** The maximum stress on the copper wire in the middle of the winding, plotted as a function of the copper fill factor and the coefficient of thermal expansion of the epoxy.

**Figure 7.** The maximum stress in the epoxy, plotted as a function of the copper fill factor and the coefficient of thermal expansion of the epoxy.

From Figure 6, it can be seen that the stress on the copper wire in the middle of the winding increases with increasing $a_{\text{epoxy}}$. Among the four copper fill factor values used in the simulations, the stress is seen to be minimal when the copper fill factor is 0.5 and this holds true for all the $a_{\text{epoxy}}$. 
Figure 7 shows that the stress on the epoxy also increases with increasing $\alpha_{epoxy}$. At lower values of $\alpha_{epoxy}$, increasing the copper fill factor does not seem to have much effect on the stress on the epoxy, but at higher $\alpha_{epoxy}$, the stress is reduced when the copper fill factor is increased. For instance, for $\alpha_{epoxy} = 100 \times 10^{-6} \, (1/K)$, when the copper fill factor is increased from 0.32 to 0.6, the maximum stress on the epoxy is decreased by about 25%.

The thermally induced mechanical stress not only depends on the difference in coefficient of thermal expansion of different materials, as seen from the results above, but also on the temperature change. This can also be understood from (1). Next, the maximum stress induced is studied as a function of the temperature. For this, several simulations are performed with different uniform temperature levels ranging from 50 to 200 °C at an interval of 25 °C. The results are shown in Figures 8 and 9, for a copper fill factor of 0.5. In Figure 8, the maximum stress experienced by the copper wire in the middle of the winding is plotted against the temperature for different values of $\alpha_{epoxy}$. Figure 8 shows the maximum stress on the epoxy plotted against the temperature. The simulated results show that the stress increases linearly with temperature. This is obvious because both the thermal expansion coefficient and the Young’s modulus of the epoxy are assumed to be constant for all the temperature levels in the simulations. But in reality, one or both of these parameters might depend on the temperature.

**Figure 8.** Maximum stress in the copper wire in the middle of the winding, as a function of temperature, for different thermal expansion coefficients of epoxy.

**Figure 9.** Maximum stress in the epoxy as a function of temperature, for different thermal expansion coefficients of epoxy.
5. Non-Uniform Temperature Distribution

Next, the thermally induced mechanical stress is studied when the stator winding segment is subjected to a non-uniform temperature distribution. The simulation procedure is the same as above. First, the thermal model is solved to obtain the temperatures in the overall volume. For this, the copper wires are treated as a heat source with a loss density of $4.1 \times 10^6$ W/m$^3$, which corresponds to the copper loss of 242 W, based on the result of a previous thermal analysis performed on the same machine [28]. The convective heat transfer coefficient is defined on the outer and the inner surfaces of the stator winding segment, based on literature [28,29]. The outer surface is considered as water cooled, with water inlet temperature 40 °C where as for the inner surface, the heat transfer coefficient is calculated based on the empirical formulas derived in Reference [29]. The adjacent sides in the circumferential direction and the rear back-face side in the axial direction are assigned with symmetric boundary conditions. The resulting temperature distribution is shown in Figure 10, which is evidently non-uniform. Then the temperature computed in the overall volume is used as an input to the structural model.

The boundary conditions in the structural model remain the same as in the previous section, also shown in Figure 2. The von-Mises stress distribution on the entire volume is shown in Figure 11. The distribution of the stress is similar to the previous case (see Figure 3). Again, the area of the stator tooth close to the windings have high stress, due to the difference in the coefficients of thermal expansion and also near the bottom corner of the tooth and the copper wire in the vicinity because of the deformation caused by the expansion.

![Figure 10. Non-uniformly distributed temperature obtained from the thermal analysis.](image)

![Figure 11. The von-Mises stress distribution over the stator segment for non-uniform temperature distribution.](image)
The stress in the windings (copper wires + epoxy) is shown in Figure 12, while the stress in the epoxy at different axial positions is shown in Figure 13. The stress distribution is similar to the previous case. The stress is relatively higher in the region between the tooth and inner layers of the winding. The stress in the region around the middle layers of wires remains small for the same reason as explained in the previous section.

![Figure 12](image-url) **Figure 12.** The von-Mises stress distribution in the winding for non-uniform temperature distribution.

![Figure 13](image-url) **Figure 13.** The von-Mises stress distribution in the epoxy at three different axial positions: 0, l/2 and l; for non-uniform temperature distribution.

Although the distribution of the stress is similar to the previous case, the magnitude of the stress is relatively higher in the tooth-winding interface. This is due to the fact that in this case, in addition to the mismatch of the coefficient of thermal expansion, the tooth and the windings are exposed to different temperature levels.

In the model that results in Figures 10–13, the copper fill factor used is 0.6 and $\alpha_{\text{epoxy}}$ is $50 \times 10^{-6}$ (1/K). Next, parametric studies based on the parameters of Table 3 are performed for the non-uniform temperature distribution. The results are shown in Figures 14 and 15. It is evident from both figures that the epoxy with low thermal expansion coefficient reduces stress significantly for all given copper fill factors. The increase in the copper fill factor is seen to have a slight effect on the stress on the copper wire in the middle of the winding, with the minimum stress being at the copper fill factor of 0.50. On the epoxy, the stress has a decreasing trend with increasing copper fill factor for all $\alpha_{\text{epoxy}}$, except at $25 \times 10^{-6}$ (1/K).
The set-up consists of one stator tooth of the switched reluctance machine, the parameters of which are listed in Table 1.

The construction of the set-up is explained figuratively in Figure 16. A concentrated winding with 36 turns in enameled copper wire of 0.9 mm diameter, with a fixed width between each turn, is wounded around the tooth. The reason for choosing a low number of turns with a fixed distance between each turn is twofold. First, it allows us to obtain a better accuracy in positioning the wires more accurately explained in section 2. Secondly, the 3D numerical model is easier to solve with a rather low number of thick copper wires than with many very thin wires. Both arguments allow us to validate the stress computed from the numerical model more accurately. As explained in section 2, the winding has a rectangular cross-section, and does not follow the curvature of the stator yoke, as is shown in Figure 2b. The winding in the set-up is impregnated with Epoxylite TSA 220S epoxy resin.

To measure the stress, two strain gauge sensors are installed on the iron surface at one end of the set-up as shown in Figure 16(2). The strain gauge sensor installed on the tooth side is denoted by Sensor 1 and the strain gauge sensor installed on the yoke side is Sensor 2.

**Figure 14.** The maximum stress on the copper wire in the middle of the winding, plotted as a function of the copper fill factor and the coefficient of thermal expansion of the epoxy when the temperature distribution is non-uniform.

**Figure 15.** The maximum stress in the epoxy, plotted as a function of the copper fill factor and the coefficient of thermal expansion of the epoxy when the temperature distribution is non-uniform.

**6. Measurement of Stress on a Segmented Stator Winding Set-Up**

In order to get an experimental assessment, the stress on a segmented stator winding is measured. The set-up consists of one stator tooth of the switched reluctance machine, the parameters of which are listed in Table 1.

The construction of the set-up is explained figuratively in Figure 16. A concentrated winding with 36 turns in enameled copper wire of 0.9 mm diameter, with a fixed width between each turn, is wounded around the tooth. The reason for choosing a low number of turns with a fixed distance between each turn is twofold. First, it allows us to obtain a better accuracy in positioning the wires in the experimental set-up. Secondly, the 3D numerical model is easier to solve with a rather low number of thick copper wires than with many very thin wires. Both arguments allow us to validate the stress computed from the numerical model more accurately. As explained in section 2, the winding has a rectangular cross-section, and does not follow the curvature of the stator yoke, as is shown in Figure 2b. The winding in the set-up is impregnated with Epoxylite TSA 220S epoxy resin. To measure the stress, two strain gauge sensors are installed on the iron surface at one end of the set-up as shown in Figure 16(2). The strain gauge sensor installed on the tooth side is denoted by Sensor 1 and the strain gauge sensor installed on the yoke side is Sensor 2.
temperature sensors are installed in the set-up, one inside the winding and other on the outer epoxy surface. The dSpace module is used for data acquisition. The complete experimental set-up is shown in Figure 17.

Figure 16. Construction of the segmented stator winding set-up: (1) 0.9 mm copper wire is wounded, having 36 turns spaced equally; (2) two strain gauges are installed on the stator segment, one beneath the yoke and one along the side of the tooth; (3) the epoxy impregnated winding is placed around the tooth; (4) the remaining space around the winding is also impregnated with epoxy.

The segmented stator winding set-up is then placed in a thermally insulated box. The winding of the set-up is fed with 5 A dc. The stress is measured at different temperature levels. Two PT100 temperature sensors are installed in the set-up, one inside the winding and other on the outer epoxy surface. The dSpace module is used for data acquisition. The complete experimental set-up is shown in Figure 17.

Figure 17. The complete experimental set-up.

As the current is supplied in the copper wires, the temperature in the set-up starts to rise. Figure 18 shows temperature rise in the two locations were the PT100 sensors are installed. The current was switched off when the temperature inside the winding reached around 106 °C. From the data acquired through the strain gauge sensors, the von-Mises stress is determined. In Figure 19, the von-Mises stresses measured by the two sensors are plotted as a function of the temperature inside the winding.
The stress measured by Sensor 1 is very high, 3–5 times higher compared to the stress measured by Sensor 2. One crucial thing to note is the non-linear behavior of the measured stress. This could be because in reality the coefficient of the thermal expansion of the epoxy could be non-linear. Although some literature reporting the non-linear thermal expansion in Aluminum alloys [30] and carbon/epoxy laminated composites [31] exist, no report was found on the behavior of epoxy resin itself. Moreover, very little data was available about the properties of the epoxy used in the measurement. Nevertheless, it is evident from the measured results that the stress increases with the increase in the temperature.

A numerical model with the geometry and the boundary condition identical to the segmented stator winding used in the experimental set-up is developed in Comsol for validation purposes. The geometry of the new model is shown in Figure 20, together with the boundary conditions used in the structural analysis. In the experiment, the set-up has a mechanically fixed surface at the end where the strain gauge sensors are installed. Therefore, one of the end surfaces (front face) in the numerical model is also modeled with a fixed boundary condition. The end windings are neglected in the numerical model. Since only one of the end surfaces is fixed, the possibility of using half the axial length with a symmetric boundary condition ceases. Therefore, a full active length of the stator tooth is used in the simulation, with a free to move boundary condition at the rear face. The model is symmetric along the XY plane. The outer surface of the epoxy is also modeled as free to move.

**Figure 18.** Temperature measured by the PT100 sensors installed inside the winding and in the outer surface of the epoxy.

![Temperature measurement diagram](image1.png)

**Figure 19.** The von-Mises stress measured by the strain gauge sensors installed in the iron surfaces. Sensor 1: Tooth side, Sensor 2: Yoke side.

![Stress measurement diagram](image2.png)
The simulation procedure is the same as described in the previous sections. First, the thermal model is solved to obtain a temperature distribution. In this case, a time-dependent temperature distribution in the overall volume is obtained. The temperatures calculated at the location of the two PT100 temperature sensors are shown in Figure 21. Although the temperature rise in the simulation is fast compared to the measurement, the time-evolution of the temperature and the difference between the temperatures inside the winding and the outer surface of the epoxy is identical to that obtained from the measurement.

The structural simulations are performed for discrete temperature levels and the stresses are obtained. Figure 22 shows the stress distribution obtained for the case when the temperature inside the winding is 106 °C. It is clear that the stress is more concentrated towards the end where the sensors are installed (towards the front face). Figure 23 shows the comparison between the simulation and the measurement. In this figure, the black line shows the stress measured by Sensor 2 installed on the yoke-side iron surface, the blue line shows the von-Mises stress computed at the sensor location and the red line shows the maximum von-Mises stress obtained in the proximity of the sensor location (in the center of the yoke-side surface close to the front face). The experimental reading from Sensor 2 shows a non-linear behavior whereas the simulated results are linear, causing discrepancies between the results. In Figure 22, it can be seen that the order of the magnitude of the stress is the same on both the tooth-side surface and the yoke-side surface. Therefore, comparing the simulated stress on the tooth-side with the stress measured by the Sensor 1 will have higher discrepancies.
Figure 22. The von-Mises stress distribution in the iron when the temperature inside the winding is 106 °C.

Figure 23. Comparison between the simulated and the measured stress in the yoke-side surface. The measured stresses are from Sensor 2.

Other than the possible non-linear thermal expansion properties of the material used in the measurements as the main reason, some discrepancies between the measured and the simulated results can also be explained as follows:

1. Set-up construction: Several cracks were seen in the outer epoxy surface, which can also be seen in Figure 16(4), forming after the curing process. Although this outer surface is quite far from the stress sensors, it may influence the temperature and stress distribution inside the windings. In addition, the position of the wires shows small deviations from the positions in the simulation (visible in Figure 16(3)), and hence the distribution of the epoxy is also influenced.

2. Assumptions in the numerical model: The end-winding region has been neglected in the numerical model. In real motors, the end-windings of the stator are not epoxy impregnated. However, in the experimental set-up, the end winding region has also been impregnated with epoxy. Neglecting this certainly affects the stress computed in the simulation. Also, the actual fixed surface in the experimental set-up is the surface of the epoxy beneath the end-windings, but the numerical model is simplified by fixing one of the axial sides of the tooth.

3. Inaccuracies in the measurement: The tolerances of the sensors together with tolerances of the components in the conditioning circuits could introduce slight errors in the measured results.
7. Conclusions

In this paper, an effort has been made to quantify the mechanical stress induced in the windings of an electrical machine due to high temperatures. This is done numerically by performing thermo-structural simulations on a segmented stator winding geometry. The simulation results are presented for both uniform and non-uniform temperature distributions in the geometry. Results show high stress in the epoxy and also in the copper wires. If the temperature is very high, the stress can reach well beyond the yield and tensile strength of the polymer coatings, which could lead to failure. Parametric studies show that the stress could be reduced by increasing the copper fill factor and using an epoxy with low thermal expansion coefficient. Measurement of stress on a segmented stator winding set-up resulted in stress comparable to that obtained from the simulations, although discrepancies were observed. Nevertheless, the measurements highlighted the non-linear thermal expansion behavior of the materials used.

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