A Photometric Study of Two Contact Binaries: CRTS J025408.1+265957 and CRTS J012111.1+272933

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Abstract

We performed new photometric observations for two contact binaries (i.e., CRTS J025408.1+265957 and CRTS J012111.1+272933), which were observed by the 1.0 m telescope at Xinjiang Astronomical Observatory. From our light curves and several survey data, we derived several sets of photometric solutions. We found that CRTS J025408.1+265957 and CRTS J012111.1+272933 were A- and W-type UMa, respectively. The results imply that the spot migrates or disappears in the two contact binaries, which were identified by chromospheric activity emissions (e.g., Hα, emission) from LAMOST spectra. From the O–C curves, the orbital periods of the two contact binaries may be increasing, which is interpreted by the mass transfer from the less massive component to the more massive one. With mass transferring, the two contact binaries may evolve from the contact configurations to semi-detached ones as predicted by the theory of thermal relaxation oscillation.

Key words: (stars:) binaries: eclipsing – (stars:) binaries: spectroscopic – stars: fundamental parameters – stars: distances – stars: individual (CRTS J025408.1+265957, CRTS J012111.1+272933)

Online material: machine-readable tables

1. Introduction

Eclipsing binaries are some of the most attractive research subjects in stellar astrophysics because they play a significant role in stellar evolution and are currently the most powerful tool to measure stellar parameters. Eclipsing binaries with light variations where there is little difference between primary and secondary eclipsing depths are referred to as W UMa systems. W UMa systems have approximately similar primary and secondary eclipsing depths are referred to as W UMa systems. W UMa systems have approximately similar temperatures in both of their components due to a common envelope (Yildiz & Doğan 2013). Normally there is contact between the two components, along with a synchronously circular orbit (Malkov et al. 2006).

W UMa systems, whose spectral classes range generally from F to K, include two late-type dwarf stars that usually exhibit stellar magnetic activities, such as starspots (Kjurkchieva et al. 2019), flares (Huang et al. 2020), chromospheric activity (Whelan et al. 2021) and magnetic activity cycles (Hu et al. 2020). The orbital periods in W UMa systems are usually short, about 0.4 days. It is noteworthy that their orbital periods are generally variational, which can be attributed to a number of factors, including the mass transfer between the two components (Hoffman et al. 2006), magnetic braking effects (Applegate 1992; Lanza et al. 1998), magnetic cycles (Borkovits et al. 2005), and the third body (Eggleton 2006; Ma et al. 2018). W UMa systems were divided into A- and W-types by Binnendijk (1970)—the hotter component has more mass in A-type systems, while W-type systems are the opposite.

The photometric data of W UMa binaries have recently been released by many surveys, such as the Wide Angle Search for Planets (SuperWASP, Street et al. 2003; Butters et al. 2010), the Catalina Sky Survey (CRTS Drake et al. 2009, 2014), the All-Sky Automated Survey for Supernovae (ASAS-SN, Jayasinghe et al. 2018, 2019; Pawlak et al. 2019; Jayasinghe et al. 2020), the Zwicky Transient Facility (ZTF, Bellm et al. 2019), and the Transiting Exoplanet Survey Satellite (TESS, Ricker et al. 2014, 2015). These surveys provide an opportunity for the study of W UMa binaries.

In this paper, we select two W UMa binaries named CRTS J025408.1+265957 (TIC 436926796, 2MASS 02540811+2659578, LPSEB19) (hereinafter as J0254) and CRTS J012111.1+272933 (TIC 16996819, 2MASS 01211118+2729334, LPSEB31) (hereinafter as J0121) from the catalog of spectral eclipsing binaries (Yang et al. 2020) to investigate their relevant properties. J0254 and J0121 were periodic variable stars (Drake et al. 2014) and were defined as typical W UMa binaries (Jayasinghe et al. 2019). J0254, with an orbital period of 0.311886 days from the International Variable Star Index (VSX) or an orbital period of 0.311858 days (Jayasinghe et al. 2019), is 14.85 or 15.19 mag in V-band mean magnitude, with amplitude

4 https://www.aavso.org/vsx/index.php?view=detail&oid=364624
of 0.71 or 0.82. Similarly, for J0121, its orbital period is 0.322818 days in VSX\(^5\) or 0.322819 days in ASAS-SN, with V-band mean magnitude of 14.92 mag and amplitude of 0.53 in VSX, or a V-band mean magnitude of 15.19 mag and amplitude of 0.57 in ASAS-SN.

In our work, we study the parameters, orbital period variation and magnetic activities of the two W UMa binary targets. The paper is organized as follows. In Section 2, we describe the information from the observations and data. The orbital periods are studied in Section 3. The chromospheric activity is researched in Section 4. The analysis of the light curve is in Section 5. In Section 6, we discuss the properties of the two targets. Finally, a summary is shown in Section 7.

### 2. Observation and Data

#### 2.1. New Observation and Data Reduction

J0254 and J0121 were observed in 2020 with the Nanshan One-meter Wide-field Telescope (Bai et al. 2020, hereafter NOWT) at the Nanshan station of the Xinjiang Astronomical Observatory, which is equipped with a standard Johnson multicolor filter system (e.g., \(UBVR\)). A CCD camera, with the pixels of 4096 \(\times\) 4136, 78' \(\times\) 78' true field, and 1'125 each pixel scale, is mounted on this telescope.

The Johnson-Cousins \(BVRI\) filters were used during our observations, with the medium scan rate mode. The observation details, such as the target name, observation date, exposure time, number of images, and mean error of photometric observation, are listed in Table 1. For J0254, a total of 492 CCD images are obtained, and another target (J0121) with 1428 CCD images. The observation precision in more than 90% is better than 0.008 mag. We note that the third observation night of J0121 is slightly less accurate than the other nights (see row 5 of the Mean Error column in Table 1), which is probably due to the weather. The observed CCD images are reduced by the standard aperture photometry package of the Image Reduction and Analysis Facility (IRAF\(^6\)) in the standard manner. The process includes image trimming, bias subtraction, flat correction, and aperture photometry. The differential photometry method is adopted in our work. The basic information about the variable stars, the comparison stars, and the check stars are compiled in Table 2, and the partial photometric data are displayed in Table 3.

#### 2.2. Survey Data

The photometric data of J0254 and J0121 are also obtained from the SuperWASP, CRTS, ASAS-SN, and ZTF survey databases. These data are characterized as follows: (a) unfiltered observation and only V-band data available in CRTS; (b) only V-band data in ASAS-SN; (c) ZTF including \(g, r\) bands for our targets; (d) the data in SuperWASP obtained by multiple times scan in same night. There are big magnitude

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5 https://www.aavso.org/vsx/index.php?view=detail.top&oid=362110

6 http://iraf.noao.edu/
SuperWASP were processed in the following steps: WASP data need to be processed. Therefore, the raw data of range of the telescope. Among these data, only the Super-
errors in the SuperWASP data for the two targets, which may be because the two targets are outside the suitable magnitude
In addition, the photometric data of the two objects are also found in TESS database. J0254 was observed in Sectors 18, 42, 43, and 44, while J0121 in Sector 17. The principal data products collected by the TESS mission exist in three forms (the Full Frame Images (FFIs), the Target Pixel Files (TPFs), and the Light Curve Files (LCFs)). Only FFIs, with a cadence of 30 minutes (Sectors 17, 18) and 10 minutes (Sectors 42, 43, 44), of both targets were available. We adopted the python package Lightkurve\footnote{\url{http://docs.lightkurve.org/}}\footnote{\url{https://docs.lightkurve.org/tutorials/2-creating-light-curves/2-3-k2-pldcorrector.html}} to reduce them and obtain the light curves for the two targets by using the PLDCorrector.\footnote{\url{http://www.lamost.org/dr7/}} The TESS data are shown in the upper panel of Figure 1. In this paper, we aim to seek the times of minima (eclipse timings) based on the data from TESS, which was used for \((O - C)\) analysis. The different methods were used to deal with the data with different cadence. The data with the 30 minutes cadence were clipped and stacked with a similar method adopted by Li et al. (2021) to obtain more times of minima.

For each observation sector, the data of 30 minutes cadence are divided into four parts among which each part was converted into one period through the equation \(BJD = BJD_0 + P \times E\), with \(BJD\) representing the observing time, \(BJD_0\) denoting the reference time, \(E\) referring to the cycle, and the orbital period indicated as \(P\). In this equation, the orbital periods of J0254 and J0121 we adopted were 0.311886 and 0.322818 days in VSX, respectively. By the method, the corresponding four diagrams of J0121 are obtained, as shown in the middle panel of Figure 1. We can also obtain times of minima on the data of 10 minutes cadence, which based on the manner, that is, the data for each sector is divided into five parts from which the light curve in one period was extracted each part. For example, we displayed the five light curves of J0254 from sector 44 in the bottom panel of Figure 1.

Except photometric data, the spectral data of the two targets can be found in LAMOST Data Release 7,\footnote{\url{http://www.lamost.org/dr7/}} with five low-resolution spectra for J0254 and two low-resolution spectra for J0121. Their spectral parameters are tabulated in Table 4, which including the object, observational date, Heliocentric Julian date, phase, spectral type, as well as effective temperature, surface gravity, radial velocity, and their corresponding errors. The phase is calculated...
based on the linear ephemeris (see more details in Section 3).

3. Orbital Period Study

In this paper, the higher temperature components of the binary systems were regarded as the primary components. With our observations, the eclipse timings were obtained through the K-W method given by Kwee & van Woerden (1956) from the BVRI-bands light curves. The new times of minima by us and their mean values are shown in Table 5.

![Figure 1](image_url)
In order to study the orbital period variations, we searched for as many eclipse timings of J0254 and J0121 as we could. Thirty-six eclipse timings of J0254 and 32 eclipse timings of J0121 were obtained from the SuperWASP database by the K-W method in Nelson’s program.10 The eclipse timings of J0254 and J0121 can also be found from Yang et al. (2020), who pointed out that these times are primary eclipse timings. In the subsequent analysis, the times of minima were transformed from MJD to HJD through the website.11 In addition, the times of minima of J0254 and J0121 were also provided by the ASAS-SN. There are not corresponding errors in the eclipsing times of minima between 2004 and 2021, which were displayed in Table 6.

We fit \((O - C)\) diagrams with the OCFit package (Gajdoš & Parimucha 2019) in which the robust regression method was employed to achieve the linear ephemeris fitting. The formula to indicate the linear ephemeris is as follows:

\[
HJD = HJD_0 + P \times E. \tag{1}
\]

### 3.1. J0254

For J0254, a total of 81 times of minima are determined, which are listed in Table 6. Based on the period of 0.3118858 days from the ASAS-SN database and all times of minima, the first linear ephemeris can be expressed as:

\[
\text{Min.1} = 2459160.22140(9) + 0.31188613(3) \times E, \tag{2}
\]

The \((O - C)_{2}\) values based on this ephemeris plotted in the left panel of Figure 2 suggests a continuously increasing period. A quadratic fit to these times of minima yields

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10 https://www.variablestarssouth.org/software-by-bob-nelson/
11 http://www.physics.sfasu.edu/astro/javascript/hjd.html
12 https://astroutilis.astronomy.ou.edu/time/bjd2utc.html (Eastman et al. 2010).
13 http://www.physics.sfasu.edu/astro/javascript/hjd.html
following ephemeris:

\[
\text{Min.I} = 2459160.22135(5) + 0.31188673(5) \times E + 4.2(3) \times 10^{-11} \times E^2,
\]

a continuous period increase ratio of \( \frac{dP}{dt} = 9.8(7) \times 10^{-8} \) days yr\(^{-1} \) is derived from the quadratic term.

### 3.2. J0121

We obtained forty-nine eclipse timings of J0121. With the period of 0.322819 days given by the ASAS-SN and all eclipse timings in Table 6, we derived the following linear ephemeris:

\[
\text{Min.I} = 2459109.42231(54) + 0.32281773(7) \times E.
\]

The \((O - C)\) diagram plotted in the right panel of Figure 2 clearly shows the signature of a linearly increasing period. The quadratic ephemeris was obtained as follows:

\[
\text{Min.I} = 2459109.42381(19) + 0.32282331(31) \times E + 3.1(2) \times 10^{-10} \times E^2,
\]

implying a continuous period increase of \( \frac{dP}{dt} = 6.9(4) \times 10^{-7} \) days yr\(^{-1} \).

For the two targets, we note that eclipse timings from Yang et al. (2020) did not correspond to the primary eclipse timings but secondary eclipse timings. The \((O - C)\) analysis suggested that the orbital period of both targets is increasing, which will be discussed in Section 6.3.

### 4. Chromosphere Activity Analysis

Chromospheric emission lines, including Ca II IRT, H\(\alpha\), H\(\beta\), H\(\gamma\), H\(\delta\), and Ca II H&K, are usually used to study whether late-type stars have chromospheric activity (Soderblom et al. 1993; Zhang et al. 2020). Our targets J0254 and J0121 have five and two low-resolution spectra from LAMOST, respectively. The low-resolution spectra of binary is represented as a common characterization of its two components. The chromosphere activity emission lines of the binary are masked by its photosphere stronger absorption lines. So the spectral subtraction technique, whose principle is that stars with similar spectral types have nearly the same level of photospheric flux, is adopted in this paper to remove the influence of the photosphere. The chromospheric flux of active stars can be estimated by subtracting that of inactive stars with similar to the spectral types of the active stars (Montes et al. 1995).

Strassmeier et al. (2000) provided a list of 750 stars with no chromospheric activity. For these 750 sources, a total of 52 spectral lines were obtained from LAMOST DR7. There are 39 spectral lines after removing poor spectral lines. The remaining lines were normalized to cross-match the seven spectral lines of the two targets, then obtained four spectra of HD 224844, HD 87680, and HD 13357. These four spectra were used to make synthetic spectra. The chromosphere activity signals of the two targets are detected by subtracting the synthesized spectra obtained from the spectra of the two targets. The results are shown in Figure 3.

To evaluate these chromospherically active emission lines, we used the PHEW\(^{14}\) package to calculate the equivalent widths (EWs) of these emission lines. The results obtained after a thousand MC iterations are listed in Table 7. Note that the low-resolution spectra are caused by the coupling of the two components of the two targets. Therefore, the spectral line broadening mechanism makes the equivalent widths

\(^{14}\) PytHon Equivalent Widths https://zenodo.org/record/47889.
corresponding to these emission lines numerically small. The characteristics of the emission lines in Figure 3 correspond essentially to their obtained equivalent widths, implying the presence of chromospheric activity in the both targets.

5. Photometric Analysis

To further investigate J0254 and J0121, we analyzed our BVRI bands light curves by using the 2013 version of the W-D program (Wilson & Devinney 1971; Wilson 1979, 1990, 2008; Wilson et al. 2010; Wilson 2012). We set the effective temperature ($T_2$) of the primary star to be the average of the spectral temperatures in Table 1, 5544 ± 148 K for J0254 and 5659 ± 35 K for J0121. Based on this temperature, the gravity-darkening coefficients and the bolometric albedo were set to $g_{1,2} = 0.32$ (Lucy 1967) and $A_{1,2} = 0.5$ (Rucinski 1969) in the both targets. The bolometric and bandpass limb-darkening coefficients are estimated from van Hamme (1993) with the square-root functions law. Due to the lack of radial-velocity data for the two targets, we determined the mass ratios $q$ of J0254 and J0121 by applying the $q$-search method to the NOWT data, and the results are shown in Figure 4. We found the smallest $\sum \omega (O - C)^2$ obtained when $q = 0.72$ for J0254 and $q = 3.05$ for J0121 after using the W-D program.

When analyzing the light curve of a binary using the W-D program, we first need to determine the contact state of the two components of the binary system. But the contact states of these two targets cannot be determined yet. So we perform the calculation using mode 2, which corresponds to the detached binary. Then we found that the two components of the two targets always fill their Roche lobes during the process of operation, which means that the binaries are the contact binaries (mode 3 in the W-D program). The adjustable parameters were the orbital inclination ($i$), the mean temperature of the secondary component ($T_2$), the monochromatic luminosity of the primary component ($L_1$) in each band of $B$, $V$, $R$, $I$, and the dimensionless potential ($\Omega_1 = \Omega_2$). The photometric elements of J0254 and J0121 are shown in Table 8. The results show that J0254 is a typical A-type W UMa contact binary, and J0121 is a W-type W UMa contact binary.

The O’Connell effect (difference in the maxima with 0.02 mag of J0254 in Figure 5), classically thought of as an indicator of spot activity. For J0254, an excellent result can be obtained by adding a cold spot to the main component. The results are shown in Table 8 and the theoretical light curves with and without spots are displayed in the left panel of Figure 5. We note that $\sum \omega (O - C)^2$ of 0.0017 acquired with the cool spot is smaller than $\sum \omega (O - C)^2 = 0.0020$ without starspot for J0254.
According to the NOWT data, we found no evidence of the presence of starspot on J0121.

We also performed the photometric analysis of CRTS, ASAS-SN, and ZTF data. Considering that the photometric light curve of CRTS and ASAS-SN was obtained at similar observation time of LAMOST spectra (from 2011 to 2014), we adopted the spot model to fit these light curves, as well as the same input parameters mentioned above. When running the program, in order to simplify the model, the spot latitude \( \phi \) is fixed at 90° (1.5708 radian) and the temperature factor \( T_J(T_d/T_0) \) is fixed at 0.8. We found the presence of a cold spot on the more massive component of J0254 based on the ASAS-SN data, but no starspot is present in the CRTS with ZTF data results. While the results of J0121 in CRTS, ASAS-SN, and ZTF data all indicate the presence of a cold spot on its massive component. The optimal results are presented in Table 9, and the fitted theoretical light curves are plotted in Figure 6. The corresponding stellar structure is presented in Figure 7.

As shown in the above results, from the CRTS and ZTF data, no starspot was found on J0254. This may be due to the fact that the two components of J0254 have similar masses, so that the chances of magnetic activity occurring in either component may be equal, which makes the dispersion increase at the two maxima of the light curve, thus masking the starspot. In conclusion, the photometric solutions for J0254 and J0121 indicate the presence of starspots. Combined with our chromospheric activity analysis, it is confirmed that the two targets have magnetic activity.

6. Discussion

In this section, we discussed absolute parameters estimation with different methods (Section 6.1), calculated the distances of the two targets (Section 6.2), and analyzed the evolution for our targets (Section 6.3).

6.1. Absolute Parameters

The absolute parameters of binary usually include mass \( M \), radius \( R \), luminosity \( L \), and the semimajor axis of the orbit \( a \). These parameters are linked to each other. In a binary system, the accurate absolute parameters can be determined in the case of having radial-velocity curves. However, in the absence of the radial-velocity curves, we can only use some estimation methods to assess the absolute parameters of the binary system.

Zhang et al. (2017) proposed a new method for estimating absolute parameters and provided mass–radius relations of two contact binary systems (GQ Boo and V1367 Tau). They

| Parameters | Values | Errors | Values | Errors |
|-----------|--------|--------|--------|--------|
| \( g_1 = g_2 \) | 0.32 | Assumed | 0.32 | Assumed |
| \( A_1 = A_2 \) | 0.5 | Assumed | 0.5 | Assumed |
| \( \Omega_{\text{rot}} \) | 3.27848 | Assumed | 6.68243 | Assumed |
| \( \Omega_{\text{out}} \) | 2.86696 | Assumed | 6.06275 | Assumed |
| \( q(M_2/M_1) \) | 0.72 | \( \pm 0.001 \) | 3.05 | \( \pm 0.0022 \) |
| \( T_1(K) \) | 5544 | \( \pm 148.12 \) | 5659 | \( \pm 35.13 \) |
| \( T_2(K) \) | 5529 | \( \pm 7.73 \) | 5448 | \( \pm 3.46 \) |
| \( \iota \) | 82.641 | \( \pm 0.17 \) | 79.099 | \( \pm 0.095 \) |
| \( \Omega_1 = \Omega_2 \) | 3.23888 | 0.00368 | 6.61727 | 0.00385 |
| \( L_{\text{B}/L_\odot} \) | 0.5782 | \( \pm 0.0024 \) | 0.3194 | \( \pm 0.0009 \) |
| \( L_{\text{V}/L_\odot} \) | 0.5772 | \( \pm 0.0019 \) | 0.3061 | \( \pm 0.0007 \) |
| \( L_{\text{K}/L_\odot} \) | 0.5766 | \( \pm 0.0019 \) | 0.2982 | \( \pm 0.0006 \) |
| \( L_{\text{I}/L_\odot} \) | 0.5762 | \( \pm 0.0021 \) | 0.2925 | \( \pm 0.0006 \) |
| \( r_1 \) (pole) | 0.3893 | \( \pm 0.0005 \) | 0.2720 | \( \pm 0.0003 \) |
| \( r_1 \) (side) | 0.4119 | \( \pm 0.0007 \) | 0.2840 | \( \pm 0.0003 \) |
| \( r_1 \) (back) | 0.4442 | \( \pm 0.0009 \) | 0.3200 | \( \pm 0.0005 \) |
| \( r_2 \) (pole) | 0.3348 | \( \pm 0.0005 \) | 0.4531 | \( \pm 0.0003 \) |
| \( r_2 \) (side) | 0.3513 | \( \pm 0.0007 \) | 0.4870 | \( \pm 0.0003 \) |
| \( r_2 \) (back) | 0.3866 | \( \pm 0.0010 \) | 0.5141 | \( \pm 0.0004 \) |
| \( f \) | 9.62% | \( \pm 0.89\% \) | 10.52% | \( \pm 0.62\% \) |
| \( \theta \) (radian) | 4.8184 | \( \pm 0.0690 \) | ... | ... |
| \( \phi \) (radian) | 1.5708 | \( \pm 0.2875 \) | ... | ... |
| \( r \) (radian) | 2.203 | \( \pm 0.0080 \) | ... | ... |
| \( T_J(T_d/T_0) \) | 0.8196 | \( \pm 0.0179 \) | ... | ... |
obtained the approximate masses and radii by using the relations to limit the almost complete stellar parameter space provided by PARSEC\(^{15}\) (Bressan et al. 2012), which include all the initial stellar masses (0.1 < \(M(M_\odot)\) < 350) and ages (6.6 < log (\(t/yr\)) < 10.13), the metallicity \(Z = 0.010 - 0.023\) are selected for GQ Boo, and \(Z = 0.0001 - 0.0700\) for V1367 Tau. They pointed out that the more massive components are more suitable than the less massive components for matching the absolute parameters, with the temperature of 200 K error being used to limit the more massive components. They also pointed out that single stars are brighter and hotter than components of the same mass in a contact binary system, that there may be some bias in the estimates using the single-star evolution procedure, and that the PARSEC program may be more applicable to detached binaries. The method is used to contact binaries resulting in biases that are within the errors of the absolute parameters obtained. The setting of the atmospheric input parameters has the most influence on this method.

Wang et al. (2019) provided a method depending on the calculation of the Roche lobes (the DCRL method), while referring to the method used by Zhang et al. (2017) as DCWD, which depends on the stellar radius obtained from the W-D code. In their paper, these two methods are used to obtain the absolute parameters of AL Cas.

\(^{15}\) Padova and Trieste Stellar Evolution Code http://stev.oapd.inaf.it/cgi-bin/cmd.

Figure 5. Theoretical and observed light curves of J0254 and J0121 obtained in this paper.

| Parameters       | J0254 | J0121 |
|------------------|-------|-------|
| \(q(M_\odot/M_\odot)\) | 0.72  | 0.72  | 3.05  |
| \(T_\odot(K)\)    | 5544  | 5544  | 5659  |
| \(T_2(K)\)        | 5410 ± 17.59 | 5287 ± 94.10 | 5430 ± 18.42 | 5436 ± 35.71 | 5498 ± 64.85 | 5442 ± 16.38 |
| \(l^o\)           | 81.859 ± 0.267 | 84.044 ± 1.707 | 82.345 ± 0.304 | 79.028 ± 0.627 | 80.162 ± 1.573 | 79.953 ± 0.442 |
| \(\Omega_1 = \Omega_2\) | 3.2486 ± 0.0078 | 3.2776 ± 0.0303 | 3.2268 ± 0.0080 | 6.6178 ± 0.0253 | 6.6715 ± 0.0479 | 6.6115 ± 0.0167 |
| \(L_{1/2}/L_c\)    | 0.6049 ± 0.0041 | 0.5772 ± 0.0231 | ... | 0.3086 ± 0.0072 | 0.2937 ± 0.0125 | ... |
| \(L_{1/2}/L_c\)    | ... | ... | 0.5960 ± 0.0038 | ... | ... | ... |
| \(r_1\)           | 0.3880 ± 0.0010 | 0.3835 ± 0.0043 | 0.3913 ± 0.0012 | 0.2724 ± 0.0018 | 0.2676 ± 0.0033 | 0.2725 ± 0.0012 |
| \(r_1\)           | 0.4102 ± 0.0014 | 0.4046 ± 0.0054 | 0.4143 ± 0.0015 | 0.2844 ± 0.0021 | 0.2786 ± 0.0038 | 0.2845 ± 0.0014 |
| \(r_2\)           | 0.4418 ± 0.0020 | 0.4342 ± 0.0072 | 0.4475 ± 0.0020 | 0.3207 ± 0.0035 | 0.3112 ± 0.0061 | 0.3209 ± 0.0024 |
| \(r_2\)           | 0.3333 ± 0.0012 | 0.3291 ± 0.0044 | 0.3366 ± 0.0012 | 0.4531 ± 0.0017 | 0.4496 ± 0.0031 | 0.4535 ± 0.0011 |
| \(r_2\)           | 0.3496 ± 0.0014 | 0.3445 ± 0.0053 | 0.3535 ± 0.0015 | 0.4869 ± 0.0022 | 0.4822 ± 0.0042 | 0.4875 ± 0.0015 |
| \(r_2\)           | 0.3839 ± 0.0021 | 0.3764 ± 0.0076 | 0.3899 ± 0.0022 | 0.5141 ± 0.0028 | 0.5081 ± 0.0052 | 0.5148 ± 0.0019 |
| \(f\)             | 0.59% ± 1.90% | 0.22% ± 7.36% | 12.55% ± 1.94% | 10.43% ± 0.408% | 1.76% ± 7.72% | 11.45% ± 2.70% |
| \(\theta\) (radian) | ... | 1.7078 ± 0.6222 | ... | 4.9995 ± 0.5052 | 4.6397 ± 0.3150 | 4.5441 ± 0.0903 |
| \(\phi\) (radian)  | ... | 1.5708 | ... | 1.5708 | 1.5708 | 1.5708 |
| \(r\)             | 0.2380 ± 0.0678 | ... | 0.1491 ± 0.0336 | 0.2233 ± 0.0325 | 0.2146 ± 0.0115 | 
| \(T_\odot(T_d/T_0)\) | ... | 0.8 | ... | 0.8 | 0.8 | 0.8 |
Lu et al. (2020) provided a general formula for the DCRL method suitable for any contact binary system. The DCRL method assumes that the radius of the companion star coincides with the effective radius of the Roche lobe \( R_{\text{L}} \) that can be obtained by the following relation (Eggleton 1983):

\[
\frac{R_{\text{L}}}{a} = \frac{0.49q^{2/3}}{0.6q^{2/3} + \ln(1 + q^{1/3})},
\]

(6)

where \( q \) is mass ratio, \( q = M_1/M_2 \) for \( R_{L1} \) and \( q = M_2/M_1 \) for \( R_{L2} \).

According to Equation (6), the mass–radius relation of DCRL was derived as:

\[
\frac{R}{R_\odot} = 2.0627 \left[ \frac{q^{1/3}p^{2/3}(q + 1)^{1/3}}{0.6q^{2/3} + \ln(1 + q^{1/3})} \right] \left( \frac{M}{M_\odot} \right)^{1/3},
\]

(7)

where \( 0 < q < 1 \), and \( P \) is the orbital period. The star parameter space is obtained by PARSEC v1.2S stellar evolution code, and the parameters are listed in Table 10. They tested 140 binary systems (76 W-type and 64 A-type systems) with sufficient spectral information and found that their method is suitable for...
short-period W UMa systems with a high mass ratio and low effective temperature. Since the fractional difference \( \frac{M_{\text{circ}}}{M_{\text{star}}} \) for all sets of parameters is found less than 2.4%, \( M_{\text{star}} \) was set as 0 by them.

In this paper, we provide a generic formulation for the DCWD method that can be used for any contact binary and requires only some of the parameters of that binary system. Combining Equation (6) with Kepler’s third law, we obtain the mass–radius relationship:

\[
\frac{R}{R_\odot} = \frac{2.4089(1 + q^{1/3})p^{2/3}}{q^{1/3}} \left( \frac{M}{M_\odot} \right)^{1/3},
\]

where \( 0 < q < 1 \), and \( r \) is the result of the ratio of the companion radius to the semimajor axis of orbit obtained by the photometric analysis using the W-D program.

The mass–radius relations J0254 and J0121 are obtained from the orbital period \( P \), the mass ratio \( q \), the ratio of radius and semimajor axis \( r = R/a \) and Equations (7) and (8).

For J0254,

\[
\frac{M_1}{M_\odot} = 0.845 50(\pm 0.00027) \left( \frac{R}{R_\odot} \right)_{\text{DCRD}},
\]

\[
\frac{M_2}{M_\odot} = 0.888 97(\pm 0.00355) \left( \frac{R}{R_\odot} \right)_{\text{DCWD}}.
\]

For J0121,

\[
\frac{M_1}{M_\odot} = 1.124 07(\pm 0.00025) \left( \frac{R}{R_\odot} \right)_{\text{DCRD}},
\]

\[
\frac{M_2}{M_\odot} = 1.170 83(\pm 0.00443) \left( \frac{R}{R_\odot} \right)_{\text{DCWD}}.
\]

In this work, we use the PARSEC program of CMD version 3.6. For its input parameter space, there are three considerations.

1. In case 1, the complete parameter space without restriction. The circumstellar dust is chosen for “No dust” mode, all the initial stellar masses \((0.1 < M < 350)\) are used. The evolution model settings use the default values. The metallicity \( Z \) is from 0.0001 to 0.06 in steps of 0.0001 and the logarithmic age is from 6.6 to 10.13 in steps of 0.05.

2. In case 2, because Yıldız (2014) indicated that the average age of W UMa systems is around 4.4–4.6 Gyr, it varies depending on type A or W, so we limit the input to ages above 10. Here, the age with logarithmic from 8 to 10.13 in steps of 0.05, other input parameters are the same as in case 1.

3. In case 3, the logarithmic age is from 8 to 10.13 in steps of 0.01, and the step of metallicity \( Z \) is 0.0001. Here, the age range is from 8 to 10.13 in steps of 0.05, other input parameters are the same as in case 1.

We floated the temperature at 300 K to constrain the PARSEC output parameters. Using the DCWD method in case 1 as an example, the results of the two targets are shown in Figure 8. Data within a triple error margin of the mass–radius relationship for both targets were used to estimate the approximate absolute parameters (mass and radius) for the more massive component. We also calculated other absolute parameters and all results are presented in Table 11.

From the results, when the parameter input space of the PARSEC program was constrained by age, the maximum range of variation of the absolute parameters was 2.8%. The parameters of the two targets have different responses for the age constraint in case 1 and case 2. From the assumptions of case 1 and case 2, the age space changes from \( 6.6 < \log(t/\text{yr}) < 10.13 \) to \( 8.0 < \log(t/\text{yr}) < 10.13 \) and the estimated parameters of J0254 decrease while those of J0121 remain the same or even increase slightly when using the DCRL method.

In contrast, when using the DCWD method, the estimated parameters of J0254 are unchanged and those of J0121 are decreased. This situation may be due to the difference in the mass ratio of the two targets, or the difference in the models, which may require more target samples to analyze the causes. The results change significantly from case 2 to case 3, where we overestimate the absolute parameters of the targets by about 10%–15% without considering metallicity, which may be caused by the reduction of the parameter space making very few data satisfying the mass–radius relationship. The absolute parameter estimation method combined with the

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**Table 10**

Parameter Space of PARSEC

| Name                      | Parameter Space | Reference |
|---------------------------|-----------------|-----------|
| Evolutionary tracks       | PARSEC version 1.2S | 1, 2, 3   |
| Photometric systems       | UBVRIJHK         | 4, 5, 6   |
| Circumstellar dust        | No dust          | 7         |
| Mass                      | \( 0.1 M_\odot < M < 350 M_\odot \) | 1, 2    |
| Age                       | \( 6.6 < \log(t/\text{yr}) < 10.13 \) | 1, 2    |
| Metallicities             | 0.0001 < Z < 0.07 | 1, 2    |
| Interstellar extinction   | \( R_v = 3.1, A_v = 0 \) | 8, 9    |

**Note.** 1 Tang et al. (2014); 2 Chen et al. (2015); 3 Chen et al. (2014); 4 Maíz Apellániz (2006); 5 Bessell (1990); 6 Bessell & Brett (1988); 7 Marigo et al. (2008); 8 Cardelli et al. (1989); 9 O’Donnell (1994).
PARSEC stellar evolution model would underestimate the parameters of the target, because the more massive part of the binary is fainter and cooler than a single star with the same mass. Thus, it is closer to the actual value without restricting the atmospheric parameters. Combining the radial velocity profiles could yield physical parameters that approximate the actual values. Therefore, it is necessary to obtain radial velocity profiles by additional spectroscopic observations.

### 6.2. Distances

Using the DCRL with DCWD method, the obtained luminosity of the more massive component of our targets J0254 and J0121 are applied to the calculation of distances. The formula used for this calculation is as follows: (a) $-2.5 \log (L/L_\odot) = M_{\text{bol}} - 4.73$ (Torres 2010), (b) $M_{\text{bol}} = M_V + BC_V$, (c) $m_V - m_{V_{\text{max}}} = -2.5 \log (L/L_\odot)$, (d) $M_V = m_V - 5 \log D + 5 - A_V$. During the calculation, some parameters are necessary, including the interstellar extinction coefficient $A_{V_{\text{IRSA}}}$ (Schlafly & Finkbeiner 2011) from IRSA database.\(^{16}\) ($A_V = 0.367$ for J0254 and $A_V = 0.226$ for J0121), the bolometric corrections from Pecaut & Mamajek (2013) ($BC_V = -0.126$ for J0254 and $BC_V = -0.146$ for J0121), and the maximum visual magnitude $m_{V_{\text{max}}}$ obtained by fitting ASASSN data ($m_{V_{\text{max}}} = 14.945$ mag for J0254 and $m_{V_{\text{max}}} = 15.005$ mag)

\(^{16}\) \url{https://irsa.ipac.caltech.edu/applications/DUST/}
for J0254). The results are listed in Table 12. In order to verify the reliability of the parameter estimation method we used and the distances obtained, we used the distances provided by Bailer-Jones et al. (2018) (hereafter BJ18), the photometric distances provided by Bailer-Jones et al. (2021) (hereafter BJ21) and the distances obtained from Gaia DR3 (Gaia Collaboration 2022) for comparison with the distances we obtained.

By comparison, we find that the obtained distances are in general agreement with the distances in the literature, which proves the validity of the method we adopted. From the results, the parameters obtained in case 1 may be closer to the actual values.

### 6.3. Mass Transfer and Evolution of Angular Momentum

In this section, we use the absolute parameters obtained by the DCWD method in the case 1 condition (see Table 11) to study the evolution of the two targets.

The $(O − C)$ analysis shows that for both J0254 and J0121, there is a long-term trend of increasing orbital periods for both systems. This phenomenon can be explained by mass transfer. The equation $(O − C) = 3M ̇/M_z$ given by Tout & Hall (1991) was used to calculate the mass transfer rate of binary. The mass transfer rates of our two targets were obtained, with J0254 $(dM_1/dt = 2.682 \times 10^{-7} M_\odot \text{yr}^{-1})$ and J0121 $(dM_1/dt = −3.603 \times 10^{-7} M_\odot \text{yr}^{-1})$. From the mass transfer rates and the mass ratio of the two targets, we suggested that both targets are transferring mass from the less massive components to the more massive components. This means that these two targets are potentially excellent targets for proving the theory of thermal relaxation oscillations (Lucy 1967; Lucy & Wilson 1979). Mass transfer from lower to higher mass components in the W UMa system leads to an increase in the orbital angular momentum. According to the thermal relaxation oscillation model, these two targets may evolve as semi-detached binaries. Our two targets have magnetic activity, so the possibility that magnetic activity plays a role in the orbital period variation cannot be denied. However, due to the insufficient accumulation of occultation times, further studies of the orbital period variation of these two targets are needed in the future.

To compare with earlier studies, we used Table 7 of Li et al. (2021), including 94 A-type systems and 85 W-type systems, to understand the evolutionary state of our two contact binaries. The M-R (mass–radius) and M-L (mass–luminosity) relations are plotted in Figure 9. As seen in the figure, in most binary systems, including both targets, the more massive part is closer to the ZAMS than the less massive part, which is different from our perception that the more massive single stars evolve faster. This phenomenon can be explained by two conjectures, one

#### Table 12

| Source       | J0254      | J0121      |
|--------------|------------|------------|
| B18          | 1093 ± 49  | 1177 ± 56  |
| B21          | 1045 ± 38  | 1205 ± 47  |
| Gaia DR3     | 1091 ± 34  | 1149 ± 44  |
| DCRL case 1  | 1003 ± 135 | 1067 ± 101 |
| DCRL case 2  | 994 ± 133  | 1068 ± 101 |
| DCRL case 3  | 973 ± 130  | 1007 ± 72  |
| DCWD case 1  | 1023 ± 136 | 1087 ± 107 |
| DCWD case 2  | 1023 ± 135 | 1076 ± 103 |
| DCWD case 3  | 992 ± 133  | 1022 ± 79  |

**Note.** 1 Bailer-Jones et al. (2018); 2 Bailer-Jones et al. (2021); 3 Gaia Collaboration (2022).
being that mass transfer leads to the mass ratio reversal (Guinan & Bradstreet 1988), and the other is the theory of thermal relaxation oscillations, where the transfer of energy from the massive component to the less massive component increases the radius and luminosity of the less massive component, and makes its own radius and luminosity decrease. J0254 is more suitable for the second conjecture explanation, while the lower-mass component of J0121 has evolved faster and has left TAMS. Therefore, J0121 is more suitable for the first explanation, the current lower-mass component is the initially higher-mass component of the binary system, and this component underwent a rapid mass transfer process when it left the main sequence phase.

The ratio of the spin angular momentum $J_{\text{spin}}$ to the orbital angular momentum $J_{\text{orb}}$ reflects the stability of the binary evolution. When $J_{\text{spin}}/J_{\text{orb}} < 1/3$, the binary is in a relatively stable evolutionary state. Yang & Qian (2015) provided the equation $J_{\text{spin}}/J_{\text{orb}} = 4/3\pi k_i (k_2 r_2)^2 q$, which allows calculating this ratio, where $r_i$ is ratio of the radius $R_i$ to the semimajor axis of the orbit $a$, and the value of $k_i^2$ is set as 0.06 (Li & Zhang 2006). According to the above equation, we obtained the ratio of the spin angular momentum $J_{\text{spin}}$ to the orbital angular momentum $J_{\text{orb}}$ for the two targets as 0.0378 (J0254) and 0.0637 (J0121), respectively. The results indicate that J0254 and J0121 are currently in a stable evolutionary state.

Eker et al. (2006) provided the correlation between the contact state and the orbital angular momentum of the binary. To investigate the contact state of the two targets, we calculate the orbital angular momentum with the equation $J_{\text{orb}} = 1.24 \times 10^{-2} \times M^{5/3} \times P^{1/3} \times q \times (1 + q)^{-2}$ given by Christopoulou & Papageorgiou (2013), where $M$ is the total mass of the system. The orbital angular momentums of our two targets were obtained, with 51.702 (J0254) and 51.429 (J0121). The relationship between $\log J_{\text{orb}}$ and $\log M$ of the two targets are shown in Figure 10. It can be seen that J0121 is a contact binary, while J0254 is a shallow contact binary, which may have evolved from short-period detached binaries by angular momentum loss.

7. Summary

We performed new photometric observations of J0254 and J0121 using NOWT. We analyzed the chromospheric activity of the two targets based on LAMOST spectroscopic data. Combining the photometric data from NOWT and the survey database, we provided the linear ephemeris of the two targets, studied their orbital period variations, and also analyzed the light curves of the two targets. We also discuss various absolute parameter estimation methods and apply them to the two targets to obtain their absolute parameters. In this paper, we compare the distances of the targets with those in the literature by calculating them.

1. According to the results of the light curve analysis, J0254 is a typical A-type W UMa contact binary, and J0121 is a W-type W UMa contact binary.
2. The results show the presence of stellar spots with chromospheric activity in both targets, which indicates the presence of magnetic activity in J0254 and J0121.
3. The $(O - C)$ analysis shows that both J0254 and J0121 exhibit a long-term increasing trend in their orbital periods, implying that both targets are transferring mass from their less massive companions to their more massive ones.
4. We also studied the evolutionary status of these two targets and found that both of them are in the evolutionary stability stage. Based on the thermal relaxation oscillation theory, we predict that these two targets will transit from the contact state to the semidetached state.

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Software: Lightkurve (Lightkurve Collaboration et al. 2018), Astropy (Astropy Collaboration et al. 2013, 2018), Astroquery (Ginsburg et al. 2019), Tesscut (Brasseur et al. 2019), Numpy (Harris et al. 2020), Matplotlib, Astropy Collaboration, Robitaille, T. P., Tollerud, E. J., et al. 2013, A&A, 558, A33

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