The non-diffractive pp cross-section and Survival Probabilities at LHC

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We present an estimate of survival probability from an eikonal mini-jet model implemented with a proposal for soft gluon resummation to all orders. We compare it with experimental data for diffractive di-jet production from LHC experiments, CMS and ATLAS, both at LO and NLO order.

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1 Introduction

In this short note, we present an estimate for survival probability factors based on the eikonal mini jet model implemented with soft gluon resummation in the infrared region, developed in [1, 2]. We call this the Bloch-Nordsieck (BN) model, as its core feature is the treatment of the infrared region through exponentiation of the divergent low frequency spectra [3].

2 The BN model for pp total cross-section and its application to SP

As the center-of-mass energy available to experimental physics increases, presently being 13 TeV at particle accelerators [4, 5, 6] and 95$^{+5}_{-8}$ TeV from cosmic ray experiments [7], estimates and models for the total pp cross-sections (elastic and inelastic) need to take into account the contribution from perturbative QCD. The proposal in [1, 2] embeds a minij-jet contribution calculated from

$$\sigma_{\text{mini-jet}}(s) = \int_{p_{t\text{min}}}^{\sqrt{s}/2} dp_t \int_1^1 dx_1 \int_1^1 dx_2 \sum_{i,j,k,l} f_{i|A}(x_1, p_t^2) f_{j|B}(x_2, p_t^2) \frac{d\hat{\sigma}^{ij}_{kl}(\hat{s})}{dp_t}. \quad (1)$$

into an eikonal formulation, where unitarity is respected and multiple parton-parton collisions can be taken into account:

$$\sigma_{\text{total}} = 2 \int d^2 b [1 - e^{-\chi_I(b,s)}] \quad (2)$$

In Eq. (1), the parton densities are standard LO DGLAP evolved with $Q^2 = p_t^2$, the parton-parton cross-section is calculated from LO QCD and the minimum parton momentum for which this equation can be used is $p_{t\text{min}} \simeq (1 \div 2)$ GeV. The impact parameter dependence in Eq. (2) is to be defined by the specific modeling, such as convolution of proton form factors or Fourier transform of soft gluon resummed contribution to single parton-parton collisions. In the BN model, as described in our most recent Ref. [3], we distinguish between soft and hard collisions. Correspondingly, we propose a $b$-distribution from proton form factors for soft collisions parametrized with no pQCD input, whereas for hard collisions, calculated through Eq. (1), the $b$-distribution matches the expression obtained through soft gluon resummation in impact parameter space. More precisely, the proposal for the average number of collisions input to calculation of the total cross-section is given as

$$2\chi_I(b, s) = \pi(b, s) = \pi_{\text{soft}}(b, s) + \pi_{\text{hard}}(b, s) = A_{FF}(b) \sigma_{\text{soft}}(s) + A_{BN}(b, s) \sigma_{\text{mini-jet}}(s) \quad (3)$$
with
\[ \mathcal{A}_{BN}(b, s) = N(s) \exp(-\int d^3\pi_g(k)[1 - e^{-ik_t b}]) \] (4)

In Eq. (3), \( \int d^2b \mathcal{A}_{BN/FF}(b, s) = 1 \), and, in Eq. (4), \( d^3\pi_g(k) \) is the single soft gluon spectrum, which, in our model, is integrated from \( k_t = 0 \) to a scale \( q_{\text{max}}(s, p_{\text{tmin}}; PDF) \), calculated in correspondence with the one gluon emission kinematics. The integral over the single gluon spectrum can be extended into the \( k_t = 0 \) limit if a suitable, integrable behavior for \( d^3\pi_g(k) \) is possible. Given the presence of the infrared cancellation through the factor between square brackets, this condition of integrability corresponds to an ansatz for the behavior of the strong coupling constant such that \( \alpha_s(k_t \to 0) \propto k_t^{-2p} \), with \( p < 1 \) [9]. For a derivation of Eq. (4), we refer the reader to [8] and references therein.

What we have presented in this section divides collisions into two simple groups, soft, and hard. The soft collisions are characterized as either constant or decreasing with energy, and corresponding to partons described in impact parameter space through the proton form factor, i.e. \( \mathcal{A}_{FF}(b) \). The hard term rises with energy, and is obtained from collisions between two perturbative partons, each one from one of the colliding protons, with b-distribution from soft gluon resummation.

### 3 Survival probability in the BN model and comparison with other models

The model outlined in the previous section can give a satisfactory description of the total cross-section, and of the inelastic non-diffractive cross-section [8]. As such, it can be used to study survival probabilities for events with no hadronic activity outside the diffractive region. Following the original proposal by Bjorken [10], we shall calculate the survival probability using the expression

\[ S^2(s) \equiv <|S(b, s)|^2> = \int d^2b \mathcal{A}(b, s) P_{\text{no-collisions}} = \int d^2b \mathcal{A}(b, s) e^{-\mathcal{P}(b,s)} \] (5)

To apply this expression to our mini jet model, we deem it necessary to distinguish between the parton distributions for soft and hard events, as they have different energy and b-dependences. In particular, at large distances, \( \mathcal{A}_{FF}(b) \) falls less rapidly than \( \mathcal{A}_{BN}(b, s) \); also, unlike \( \mathcal{A}_{BN}(b, s) \), the former carries no energy dependence, as one can see in the left panel of Fig. [1].

In [8], we have proposed to “weigh” these different possibilities according to the different soft and mini-jet type contributions as in the following expression:

\[ S^2_{\text{total}}(s) = \frac{\sigma_{\text{soft}}(s)}{\sigma_{\text{soft}}(s) + \sigma_{\text{mini-jet}}(s)} <|S(b)|^2>_{\text{soft}} + \frac{\sigma_{\text{mini-jet}}(s)}{\sigma_{\text{soft}}(s) + \sigma_{\text{mini-jet}}(s)} <|S(b)|^2>_{\text{hard}} \] (6)
with
\[ < |S(b)|^2 >_{soft/hard} = \int d^2 b A_{FF/BN}(b, s) e^{-\pi_{soft/hard}(b, s)} \] (7)

In the context of mini-jet inspired models, the possibility of a mixed expression has also been considered, i.e.
\[ S^2(s) \equiv < |S(b, s)|^2 > = \int d^2 b A_{soft}(b, s) P_{no-collisions} = \int d^2 b A_{soft}(b, s) e^{-\pi(b, s)} \] (8)
such as in [10, 13, 14], with \( P_{no-collisions} \) obtained from a one-channel eikonal formulation and, in the case of [13], \( A_{soft}(b, s) \) obtained from the quark-quark contribution, which is either a constant or decreasing with energy. This expression would correspond to eliminating all hadronic events for which the parton distribution is of the form-factor type - carrying no energy dependence. For the BN model, this corresponds to eliminating all non-diffractive hadronic events, as we have mentioned. In the right panel of Fig. 1 we show our estimate from Eqs. (6) and (8), together with results from [10, 13], and those from the model (favorite estimate) of Khoze, Martin and Ryskin (KMR) [15]. For comparison with KMR results as well as those from [16], see Ref. [8].

Figure 1: Left: soft and hard parton distribution in b-space. Right: our proposal for the Survival Probability compared to estimates from CMS [11] and ATLAS [12] extracted from diffractive jet production at LHC, and with three other models: Block’s proposal in [13], a 2008 application of the BN-model from [14], estimates from Khoze, Martin and Ryskin (KMR) [15], and the Bjorken estimate [10]. For our present estimate, two different PDFs parametrizations are used, GRV and MSTW, spanning the indicated bands. Further details and references can be found in Ref. [8].
3.1 Comments about applicability of the model

The model outlined in the previous section can give a satisfactory description of the total cross-section, and of the inelastic non-diffractive cross-section, since its present one-channel formalism for the inelastic cross-section does not include the diffractive component. As a consequence, our estimates for the SP refer to experimental set-ups where only non-diffractive events are excluded.

The pQCD description of the diffractive contribution has different energy behavior than the one from parton-parton collisions. Parametrizations of the contribution to Single Diffractive events obtained through multichannel versions of the Glauber model, indicate that these contributions rise like $\log s$ [17]. Experimentally, these events are also different, since they are correlated with one of the outgoing protons, peaking in a large rapidity region.

Using this model, we have addressed here the question of how different impact parameter distributions affect estimates for survival probability in eikonal mini-jets models. There are noticeable quantitative and qualitative differences between the two sets of theoretical predictions for SP. They reflect whether all hadronic activity beyond single diffraction has been removed or not.

So far, reported SP data exist only upto 7 $TeV$ showing little or no variations with energy. Data at 8 & 13 $TeV$ would also help resolve whether there is a sharp decline or not in SP for increasing energy.

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