SPITZER SPECTRAL LINE MAPPING OF SUPERNOVA REMNANTS. I. BASIC DATA AND PRINCIPAL COMPONENT ANALYSIS

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ABSTRACT
We report the results of spectroscopic mapping observations carried out toward small (1′ × 1′) regions within the supernova remnants W44, W28, IC 443, and 3C 391 using the Infrared Spectrograph (IRS) of the Spitzer Space Telescope. These observations, covering the 5.2–37 μm spectral region, have led to the detection of a total of 15 fine-structure transitions of Ne+, Ne++, Si+, P+, S, S++, Cl+, Fe3+, and Fe6++; the S(0)–S(7) pure rotational lines of molecular hydrogen; and the R(3) and R(4) transitions of hydrogen deuteride. In addition to these 25 spectral lines, the 6.2, 7.7, 8.6, 11.3, and 12.6 μm PAH emission bands were also observed. Most of the detected line transitions have proven strong enough to map in several sources, providing a comprehensive picture of the relative distribution of the various line emissions observable in the Spitzer IRS bandpass. A principal component analysis of the spectral-line maps reveals that the observed emission lines falls into five distinct groups, each of which may exhibit a distinct spatial distribution: (1) lines of S and H2(J > 2); (2) the H2 S(0) line; (3) lines of ions with appearance potentials less than 13.6 eV; (4) lines of ions with appearance potentials greater than 13.6 eV, not including S++; (5) lines of S++. Lines of group 1 likely originate in molecular material subject to a slow, nondissociative shock that is driven by the overpressure within the supernova remnant, and lines in groups 3–5 are associated primarily with dissociative shock fronts with a range of (larger) shock velocities. The H2 S(0) line shows a low-density diffuse emission component and, in some sources, a shock-excited component.

Subject headings: ISM: abundances — ISM: clouds — ISM: molecules — molecular processes — shock waves

1 INTRODUCTION

Supernovae have long been recognized as a critical source of energy input to the interstellar medium (ISM; e.g., Cox & Smith 1974; McKee & Ostriker 1977). They send shock waves propagating through the ISM, creating large cavities filled with hot ionized material. Eventually, supernova-driven shock waves become radiative, emitting strong line emissions, primarily at optical and ultraviolet wavelengths, that have been widely observed from supernova remnants (e.g., Weiler & Sramek 1988). Where supernova remnants encounter molecular clouds, they drive slower shock waves that compress and heat the molecular material and result in strong infrared line emission. Depending on the shock velocity, such shock waves may be either dissociative, resulting in the destruction of molecules by collisional processes, or nondissociative, in that molecules are heated but nevertheless survive the passage of the shock front. The theory of interstellar shock waves, both in atomic and molecular media, has been the subject of extensive investigation (reviewed, for example, by Draine & McKee 1993).

Using the Infrared Spectrograph (IRS) of the Spitzer Space Telescope, we have carried out infrared spectroscopic observations of four regions in which a supernova remnant interacts with a molecular cloud: W44, W28, 3C 391, and IC 443. The IRS covers the 5.2–37 μm region with unprecedented sensitivity, providing access to the lowest eight pure rotational transitions of molecular hydrogen together with fine-structure lines of [S ii] and a variety of atomic ions. In the observations reported here, IRS spectroscopy indicated the presence of interstellar gas over a huge temperature range, from ≤100 K [H2 S(0) 28 μm line] to ≥103 K ([Ne iii] 15.6 and 36 μm lines).

In this paper we present a general overview of the data set we have obtained toward these four supernova remnants. In §2 we give a brief overview of the four supernova remnants selected for this study. In §3 we discuss the observations and methods used to reduce the observational data, and we present spectral-line maps for a representative sample of the transitions that we detected. In §4 we describe how principal component analysis can be used to identify distinct groups of transitions that share a common origin in a particular component of the interstellar gas. In §5 we discuss the similarities and differences in the spatial distributions of the various spectral lines we observed. More detailed analyses of the different shocked-gas components will follow in future papers.

2 SOURCE SELECTION

The four supernova remnants (SNRs) we have observed, W44, W28, 3C 391, and IC 443, represent classic examples of the interaction between supernova-driven shock waves and molecular clouds. Brief descriptions of each source are given below, and finder charts appear in Figures 1–4. In each source, we have centered the mapped region at a position that is known from previous observations to be a luminous source of molecular emissions; these are all positions that have been observed previously by the Short- and/or Long Wavelength Spectrometer of the Infrared Space Observatory (ISO). All four sources lie close to the Galactic plane, with the mapped regions lying at Galactic latitudes b ~ −0.43°, −0.30°, 0.03°, and 3.02°, respectively, for W44, W28, 3C 391, and IC 443 (see Table 1).
W44 lies at a distance of 2.5 kpc and has a radius of 11-13 pc (Cox et al. 1999). The remnant is associated with the pulsar B1853+01, which is believed to be the progenitor star and provides an age of 20,000 yr (Wolszczan et al. 1991; based on the ratio of the pulsar period to the period derivative). W44 is a prototype for a new class of SNRs called “mixed-morphology” SNRs, because the radio continuum images exhibit a shell-like morphology, while the center is filled in with X-ray emission (Jones et al. 1993; Rho & Petre 1998). Such morphologies have been attributed to the interaction between the supernova shock front and a molecular cloud (Chevalier 1999; Yusef-Zadeh et al. 2003), and W44 is indeed associated with a giant molecular cloud, recently mapped in CO emission (Reach et al. 2005, hereafter RRJ05).

RRJ05 and Cox et al. (1999) provide nice summaries of the available observations. In general, there is strong evidence for supernova interaction with a dense molecular cloud through the detection of OH 1720 MHz maser emission, broad (FWHM ~ 20–30 km s⁻¹) CO molecular line emission, vibrational and rotational lines of molecular hydrogen, and atomic fine-structure lines (Claussen et al. 1997; Seta et al. 1998; Reach & Rho 2000; RRJ05). The observations are consistent with the predictions of models that invoke a mixture of dissociative and nondissociative shocks impacting on gas with densities of 10⁰–10⁴ cm⁻³ (Reach & Rho 2000; RRJ05), although Cox et al. (1999) present a model...
Kinematic considerations based on molecular line broadening place the remnant at a distance of 1.9 ± 0.3 kpc (Velázquez et al. 2002). The distribution of radio molecular emission lines indicates that the remnant has an irregular shell-like structure with prominent peak emissions in the northern and northeast sides of the shell where an interaction between the remnant and a nearby molecular cloud was suggested (Wootten 1981). Further evidence for such an interaction arises from the detection of numerous discrete OH 1720 MHz maser spots along the northeast ridge where the remnant is believed to be interacting with a molecular cloud (Claussen et al. 1997). This maser activity has been shown to constitute a tracer of SNR--molecular cloud interaction (Yusef-Zadeh et al. 2003). Detection of the H$_2$ S(3) and S(9) lines as well as a number of ionic species with ISO suggests the presence of shocks in the northern part of the remnant (Reach & Rho 2000) as well. In the optical, short emission filaments are observed superposed over a more diffuse and centrally peaked emission seen throughout most of the interior of W28 (van den Bergh 1973; Long et al. 1991). Diffuse thermal X-ray emission is also seen throughout the region delineated by the radio shells and shows a rather patchy but centrally peaked emission distribution (Dubner et al. 2000; Rho & Borkowski 2002). Like W44, W28 shows a mixed morphology that combines a shell-like radio structure with a centrally filled diffuse X-ray emission structure. Observations of optical [S ii] line ratios (Long et al. 1991) suggest a reddening of $E(B-V)$ ∼ 1–1.3 mag, corresponding to a visual extinction of 3–4 mag for an $A_V/E(B-V)$ ratio of 3.1.

2.3. 3C 391

3C 391 (G31.9+0.0) is an X-ray– and radio-bright SNR that lies in the Galactic plane. The X-ray emission is diffuse (i.e., no limb brightening) and centered within the radio shell (Rho & Petre 1996). $^{12}$CO $J = 1−0$ maps toward 3C 391 reveal the presence of moderately dense $n$(H$_2$) ∼ 300–1000 cm$^{-3}$ molecular gas along the northwest portion of the remnant (Wilner et al. 1998). The radio continuum emission from the remnant (Reynolds & Moffett 1993), shown in Figure 3 with the region mapped by Spitzer superposed, suggests evolution along a strong density gradient, with compression of the supernova blast wave to the northwest in the direction of the strongest CO emission and lower continuum surface brightness emission to the southeast away from the molecular gas. It is likely that the progenitor star exploded

![Image](image-url)
within a dense molecular cloud and the expanding gas has now broken out of the cloud to the southeast.

Evidence exists for both dissociative and nondissociative shocks toward 3C 391 (Reach et al. 2002). Narrowband filter images in the [Fe II] 1.64 μm line show a pronounced intensity peak along the bright radio bar (18°49′16″, −05°50′00″) at the interface between the SNR and the molecular cloud. Similarly, the ISO/MIV CVF 5–18 μm spectrum of the same region is dominated by emission lines from atomic ions, such as [Fe II] 5.5 μm, [Ar II] 6.9 μμm, [Ne i] 12.8 μm, and [Ne ii] 15.5 μm, while the mid-infrared H2 rotational lines in the same spectrum are either weak or absent (Reach et al. 2002). Approximately 2.8′ to the south and east of this position, near α = 18°49′22″, δ = −05°57′22″ (J2000.0), continuum-subtracted H2 2.12 μm images show an ~30′′ diameter area containing a cluster of (≤5′′) clumps of H2 emission. The ISO/MIV CVF spectrum of this region shows strong H2 S(2) through S(7) H2 line emission (Reach et al. 2002). Longer wavelength ISO LWS spectra toward this location show thermal H2O, OH, high-J CO (Reach & Rho 1998), and [O I] 63 μm (Reach & Rho 1996) emission. This so-called broad molecular line region (see Reach & Rho 1999) is also the site of OH 1720 MHz maser (Frail et al. 1996) and broad (FWHM ~ 20 km s−1) CO (J = 2–1), CS (J = 3–2), CS (J = 5–4), and HCO+ (J = 1–0) emission (Reach & Rho 1999). The existence of strong and broad molecular line emission has led to the conjecture that the supernova blast wave is encountering dense [n(H2) ~ 104–105 cm−3] cores present within the molecular cloud from which the progenitor of 3C 391 formed. The region that we have mapped with Spitzer (Fig. 3) is centered on the broad molecular line region.

The extinction to 3C 391 is very high due to its location in the Galactic plane and its 9 kpc distance (Caswell et al. 1971; Radhakrishnan et al. 1972). Column densities inferred from the spectral analysis of Röntgensatellit (ROSAT) data yield a foreground column density of (2–3.6) × 1022 cm−2 (Rho & Petre 1996). Since this analysis has been applied by averaging spectra obtained over relatively large areas of the remnant, it is likely that the higher value applies to the denser broad molecular line region of interest here. Thus, assuming a foreground column density of 3.6 × 1022 cm−2, a line-of-sight visual extinction of AF = 19 mag is derived (Reach et al. 2002).

2.4. IC 443

IC 443 is a well-studied SNR located in the outer Galaxy at a distance of approximately 1.5 kpc (Georgelin 1975; Fesen & Kirshner 1980; Fesen 1984). It is one of the most striking examples of the interaction of a SNR with the interstellar medium. IC 443C, the position that we have targeted with Spitzer, is one of several shocked-gas regions within the SNR first identified by DeNoyer (1978) based on the presence of high-velocity H I emission. These shocked-gas regions were later detected to have broad OH absorption and CO emission lines (DeNoyer 1979a, 1979b). More extensive observations of CO and HCO+ emission in IC 443 by Dickman et al. (1992) revealed many more regions of broad molecular line emission and showed that they formed an expanding, tilted ring. This ring of shocked gas presumably delineates where the SNR shock has encountered the molecular interstellar material. This ring is also seen in 2 μm H2 emission (Burton et al. 1988; Richter et al. 1995a).

Based on the kinematics of the observed CO and HCO+ emissions, IC 443C is believed to be located on the front side of the expanding ring (Dickman et al. 1992). The unshocked molecular gas in this direction has a vLSR of ~3 km s−1. The broad velocity emission from the shocked molecular gas extends from the velocity of the unshocked gas to a vLSR of ~70 km s−1 (Snell et al. 2005). The region of most intense molecular broad-line emission is about 1′ in size.

Emission from the shocked interstellar gas in IC 443 has been extensively studied and detected in numerous atomic and molecular tracers, including H I (Braun & Strom 1986), vibrationally excited H2 (Burton et al. 1988), the 63 μm line of [O I] (Burton et al. 1990), the pure rotational lines of H2 (Richter et al. 1995b; Cesarsky et al. 1999), and numerous molecular species (DeNoyer & Frerking 1981; Ziurys et al. 1989; van Dishoeck et al. 1993). Most recently, the detection of water was reported in several of these shocked regions, including IC 443C (Snell et al. 2005). Most studies have concluded that a combination of shocks is needed to explain the emission seen in these atomic and molecular tracers. Snell et al. (2005) suggested the presence in IC 443C of both a fast J-shock and either a slow C-shock or slow J-shock. Given the observed ratio of H2 vibrational lines, Richter et al. (1995a) derived 2.1 μm extinctions of 1.3 and 1.6 mag for two slit positions in IC 443C, corresponding to visual extinctions AF of 12 and 15 mag.

3. OBSERVATIONS AND RESULTS

W44, W28, 3C 391, and IC 443C were each observed using the IRS as part of a Cycle 2 General Observer Program, the short-low (SL), short-high (SH), and long-high (LH) modules being used to obtain complete spectral coverage over the wavelength range available to IRS. The spectral resolving power of IRS, R = λ/Δλ, ranges from 60 to 127 for the SL module and is ~600 for the SH and LH modules. Spectral-line maps of size ~1′ × 1′ were obtained by stepping the slit perpendicular to its long axis by one-half its width and, in the case of SH and LH, parallel to its long axis by 4/5 of its length. Table 1 summarizes the observational details for each source; note that the map center positions are not in all cases identical to the (0, 0) positions defined in the legends to Figures 10–13.

The data were processed at the Spitzer Science Center (SSC), using version 13.2 of the processing pipeline and then reduced further using the SMART software package (Higdon et al. 2004), supplemented by additional routines (Neufeld et al. 2006b), which provide for the removal of bad pixels in the LH and SH data, the calibration of fluxes obtained for extended sources, the extraction of individual spectra at each position sampled by the IRS slit, and the creation of spectral-line maps from the set of extracted spectra. No background subtraction could be performed, since no off-source measurements were made; while background subtraction might have affected the measured continuum fluxes, it would be expected to have no effect on the derived intensities for spectral lines. There is no evidence for fringing in any of the spectra.

For several transitions observed in the LH and SH modules, the resultant line maps exhibited striping perpendicular to the long axis of the slit. We determined this effect to be an artifact created by the standard algorithm used in the IRS CLEAN software to obtain interpolated data for bad pixels; that algorithm interpolates in the dispersion direction, causing a systematic underestimate in the intensity when a bad pixel falls close to the central wavelength of a spectral line. The striping was successfully removed by applying a correction factor, computed separately for each position along the slit and for each affected spectral line. The required correction factors were obtained by considering, separately for each of the five positions along the slit, the cumulative distribution functions for the line fluxes obtained over the entire map. In other words, for each possible positions along the slit, we plotted the fraction of line flux measurements that were smaller than a given value, as a function of that value. Making the assumption that the cumulative distribution functions should be
similar except for the highest flux values, we computed the necessary correction factors needed to bring the five distribution functions into agreement.

In order to improve the signal-to-noise ratio beyond that obtained at a single position, we have computed average spectra for each of the sources we observed. The resultant spectra, plotted in Figures 5, are the averages of all spectra within a circular region, the contributing spectra being weighted by a Gaussian taper (HPBW of 25′) from the center of each synthesized beam. The central positions are given in the figure captions.

The spectra plotted in Figures 5–8 reveal a total of 25 spectral lines, detectable in one or more source. These include 15 fine-structure transitions of the species Ne+, Ne++ (two transitions), Si+, P+, S, S++ (two transitions), Cl+, Fe+ (five transitions), and Fe++; eight transitions of H2 [the S(0) through S(7) pure rotational transitions], and the R(3) and R(4) transitions of HD (detected
Fig. 6.—Same as Fig. 5, but for a 25° (HPBW) diameter circular aperture centered at $\alpha = 18^h01^m52.3^s$, $\delta = -23^\circ19'25''$ (J2000.0) in W28 [corresponding to offset (0'', 0'') in Fig. 11].
Fig. 7.—Same as Fig. 5, but for a 25° (HPBW) diameter circular aperture centered at \( \alpha = 18^h49^m21.9^s, \delta = -0^°57'22'' \) (J2000.0) in 3C 391 [corresponding to offset (0°, 0°) in Fig. 12].
Fig. 8.—Same as Fig. 5, but for a 25" (HPBW) diameter circular aperture centered at α = 06h17m42.5s, δ = +22°21'29" (J2000.0) in IC 443C [corresponding to offset (−24", −20") in Fig. 13].
Beam-averaged line intensities, in a 25" (HPBW) Gaussian Beam

| Transition | Wavelength (µm) | Intensity (10^{-6} ergs cm^{-2} s^{-1} sr^{-1}) |
|------------|----------------|-----------------------------------------------|
|            |                | W44 | W28 | 3C 391 | IC 443C |
| H₂ S(0) J = 2–0............ | 28.2188 | 7.6 | 36.2 | 12.7 | 12.9 |
| H₂ S(1) J = 3–1............ | 17.0348 | 113 | 275 | 60.3 | 359 |
| H₂ S(2) J = 4–2............ | 12.2786 | 135 | 392 | 81.7 | 499 |
| H₂ S(3) J = 5–3............ | 9.6649 | 324 | 622 | 151 | 1930 |
| H₂ S(4) J = 6–4............ | 8.0251 | 247 | 233 | 143 | 896 |
| H₂ S(5) J = 7–5............ | 6.9095 | 808 | 589 | 661 | 2331 |
| H₂ S(6) J = 8–6............ | 6.1086 | . . . | . . . | . . . | 491 |
| H₂ S(7) J = 9–7............ | 5.5112 | 436 | 231 | 272 | 1087 |
| HD R(3) J = 4–3............ | 28.502 | 5.2 |
| HD R(4) J = 5–4............ | 23.034 |
| S 3P_1–3P_0.............. | 25.2490 | 1.7 | 16.2 | 26.8 | 30.3 |
| Si^+ 2P^+_{2–2}P^+_{12}........ | 34.8141 | 149 | 415 | 835 | 973 |
| P^+ 3P_2–3P_1.............. | 32.8709 | 1.7 | 4.4 | 11.9 | 2.8 ± 0.4^a |
| Cl^+ 3P_1–3P_0............. | 14.3678 | 1.6 ± 0.5 | 3.3 | 8.6 | <1.2 (3 σ) |
| Fe^+ 4P_{12–4}D_{02}........ | 5.3403 | 107 | 151 | 386 | 316 ± 5.0 |
| Fe^+ 4F_{22–4}F_{02}........ | 17.9363 | 4.7 | 8.7 | 42.0 | 2.5 |
| Fe^+ 4P_{32–4}P_{02}........ | 24.5186 | 0.7 ± 0.12 | 2.5 | 12.5 | <1.2 (3 σ) |
| Fe^+ 4D_{22–4}D_{02}........ | 25.9882 | 22.4 | 44.7 | 160.4 | 11.3 |
| Fe^+ 4D_{02–4}D_{02}........ | 35.3491 | 5.3 | 11.6 | 47.2 | 10.3 |
| Ne^+ 3P_1–3P_0............ | 12.8149 | 156 | 247 | 538 | 15.5 |
| Ne^+ 3P_1–3P_0............ | 15.5545 | 17.1 | 38.4 | 202 | 4.2 |
| Ne^+ 3P_1–3P_0............ | 36.0135 | <2.6 (3σ) | 3.4 ± 1.1 | 18.0 | <0.9 (3 σ) |
| S^+ 3P_2–3P_1............. | 18.713 | 34.4 | 40.4 | 76.9 | <1.4 (3 σ) |
| S^+ 3P_2–3P_1............. | 33.480 | 43.7 | 74.2 | 140 | <4 (3 σ) |
| Fe^+ 3D_{22–3}D_{42}........ | 22.925 | 1.2 ± 0.2 | 3.5 | 7.1 | <0.5 (3 σ) |

^a The H₂ S(6) line intensity cannot be determined reliably, because the line is blended with a strong 6.2 µm PAH feature.

^b Error bars, when given, are 1 σ statistical errors. When error bars are not given, the uncertainty is dominated by systematic errors, which we estimate to be ≤25% (see Neufeld et al. 2006b).

4. PRINCIPAL COMPONENT ANALYSIS

A cursory inspection of Figures 10–13 reveals both similarities and differences in the spatial distributions of the various emission lines that we have observed. The method of principal component analysis (PCA) provides a valuable tool for describing those similarities and differences. The value of PCA in analyzing multi-transition maps was first demonstrated by Ungerechts et al. (1997), who applied the method to molecular line maps of the Orion Molecular Cloud and gave a comprehensive description of PCA that will not be repeated here (see also Heyer & Schloerb 1997). To summarize, PCA creates an orthogonal basis set of lines that we have observed. The method of principal components (PC), such that each observed map can be represented as a linear combination of the PC. The key feature of the new basis set is that the PC are obtained in decreasing order of amplitude; the first PC contains as much of the spatial variation as possible, the second PC (constructed orthogonal to the first) contains as much of the remaining variation as possible, and so forth.

Following Ungerechts et al. (1997), we applied the PCA to spectral-line maps that had been mean-subtracted and divided by the standard deviation, the latter being dominated by structure in the source rather than instrumental noise. This procedure gives equal weighting to each line instead of allowing the brightest lines to dominate the analysis. Because this analysis involves data obtained with all three modules (i.e., SL, SH, and LH), it was applied only to the intersection of the regions mapped by the different modules. Applying PCA to the four sources we have observed, we find that the first PC contains 58%–73% of the total spatial

toward IC 443C and reported previously by Neufeld et al. (2006a)). Beam-averaged intensities are listed in Table 2. In addition to these emission lines, the 6.2, 7.7, 8.6, 11.3 and 12.6 µm PAH emission bands are readily apparent in the spectra of W44, W28, and 3C 391, and the 11.5 µm feature is detected in IC 443C. A discussion of the PAH emission features is deferred to a future paper.

The observed line transitions represent a wide variety of excitation conditions. In Figure 9, we show their position in a scatter plot, where the horizontal axis shows the appearance potential, equal to zero for neutral species and equal to the ionization potential of X^(n–1)^+ for the case of ion X^+ and, the vertical axis shows the critical density at which the rate of collisional de-excitation equals the spontaneous radiative rate. In computing the critical density, we assumed the dominant collision partner to be electrons for ionized species and hydrogen molecules for neutral species.

In Figures 10–13, again for each source, we present maps of a representative selection of six strong spectral lines; the H₂ S(0), [S i] 25 µm, H₂ S(2), [Si ii] 35 µm, [Ne ii] 12.8 µm, and [S ii] 33 µm lines. As demonstrated by the principal component analysis described in § 4 below, each of the other transitions shows a spatial variation that is almost identical to one of the transitions plotted in Figures 10–13. For example, except for a constant scaling factor, the [Fe ii] 26 µm line maps are visually indistinguishable from those shown here for [Si ii] 35 µm. For the maps obtained with the SL module, the effective integration time and resultant signal-to-noise ratio is the same everywhere in the map. For the SH and LH modules, the effective integration time is constant, except in overlap regions between adjacent pointings where the integration time is larger by a factor 2.
variation in the maps, the first and second PCs together contain 82%–88%, and the first three PCs contain 90%–93% of the information. In Figures 14–17 we present the results of the PCA for each source. The top panel shows the fraction of the variance accounted for by each component (asterisks), along with the cumulative fraction for the first $n$ components as a function of $n$ (squares). The bottom panels show the coefficients for the first, second, and third PC needed to approximate the maps of each transition; the coefficients for the first and second PC are shown in the bottom left panel and those for the second and third PC are shown in the bottom right panel. (These figures were referred to as $h$-plots by Ungerechts et al. [1997].) Because the PCA is applied to mean-subtracted line maps, the coefficients may be either positive or negative. While the third PC contains information about the source, as evidenced by the fact that transitions with similar coefficients for the second PC tend to show similar coefficients for the third, the fourth and higher PCs are likely dominated by noise.

The principal components are normalized such that quadrature sum of the coefficients for each transition is unity. Thus, if a particular transition were completely accounted for by the first and second PC, its position in the bottom left plot would lie on the circle of unit radius; similarly, if a particular transition were completely accounted for by the second and third PC, its position in the bottom right plot would lie on the circle of unit radius. The proximity of most points in the bottom left plot to the circle of unit radius is a reflection of the fact that the first two PCs account for $\sim 85\%$ of the variance in the observed line maps. In the limit where two points actually lie on the unit circle, the cosine of the angle between the two radii measures the degree of linear correlation; points lying next to each other on the unit circle would be perfectly correlated ($\cos \theta = +1$), while those lying exactly on opposite sides of the circle would be perfectly anticorrelated ($\cos \theta = -1$). For example, in W44, the bottom left panel indicates that the $[\text{Fe}^\text{II}]$ 26 m and $[\text{Si}^\text{II}]$ transitions are very well correlated, strongly anticorrelated with both observed $[\text{S}^\text{III}]$ transitions, and almost uncorrelated with the $\text{H}_2$ S(0) transition.

In W44 the PCA yields a clear separation into five groups of spectral lines: (1) lines of S and $\text{H}_2 (J > 2)$; (2) the $\text{H}_2$ S(0) line; (3) lines of ions with appearance potentials less than 13.6 eV ($\text{Fe}^+, \text{Si}^+, \text{and P}^+$); (4) lines of ions with appearance potentials less than 13.6 eV; and (5) lines of ions with appearance potentials greater than 13.6 eV.
greater than 13.6 eV (Ne$^+$, Ne$^{++}$, and Fe$^{++}$), not including S$^{++}$; and (5) lines of S$^{++}$. In the other sources, some of these groups share a common distribution, but in no case do the spectral lines within a group defined above fail to be strongly correlated with each other. In W28 lines in groups 1 and 2 share a similar distribution, which is markedly different from that of groups 3–5. In 3C 391 lines in groups 1, 2, 3, and 5 show distributions that are readily distinguishable from each other, but group 4 shows a distribution that is very similar to that of group 3. In IC 443, groups 1, 3, and 4 are readily distinguishable from each other; group 2 [the H$_2$S(0) line] has a similar distribution to that of group 1; and group 5 ([S iii] transitions) is not detected. These behaviors suggest that the line emissions we have observed originate in at least five physically distinct components (some of which have similar distributions, as projected onto the sky, in sources other than W44). The implications of these groupings are discussed further in §5 below.

5. DISCUSSION

5.1. Line Emission from Neutral Species: H$_2$ and Atomic Sulphur

Each of the sources we observed shows strong emission in the H$_2$ S(0) through S(7) lines. In Figure 18 we present rotational diagrams derived from the H$_2$ line fluxes listed in Table 1. Here we corrected for extinction, adopting the foreground extinction estimates given in §2 and the interstellar extinction curves of Weingartner & Draine (2001; “Milky Way, $R_V = 3.1$”). The rotational diagrams bear a strong similarity to those obtained previously from Spitzer observations of the Herbig-Haro objects HH 54 and HH 7 (Neufeld et al. 2006b). In each case, a positive curvature in the rotational diagrams indicates the presence of an admixture of gas temperatures, while a characteristic zigzag pattern, more pronounced for low-lying transitions, indicates a nonequilibrium ortho-to-para ratio (OPR), smaller than 3. In Neufeld et al. (2006b), we argued that the nonequilibrium H$_2$ OPRs were consistent with shock models in which the gas is warm for a time period shorter than that required for reactive collisions between H and para-H$_2$ to establish an equilibrium OPR.

As in Neufeld et al. (2006b), we obtained a two-component fit to the rotational diagrams, in which a warm component with temperature, $T_w$, ortho-to-para ratio, OPR$_w$, and column density $N_w$ coexists with a hot component with temperature, $T_h$, ortho-to-para ratio, OPR$_h$, and column density $N_h$. The resultant parameters, listed in Table 3, are broadly similar to those obtained for HH 7 and HH 54, and are consistent with the presence of nondissociative shocks of velocity 10–20 km s$^{-1}$. Our two-component fits are

\[\text{Fig. 10.—H}_2\text{ S}(0), \text{H}_2\text{ S}(1), [\text{S i}], [\text{Si ii}], [\text{Ne ii}], \text{and [S iii]} \text{ emission-line intensities observed toward W44. The inset boxes demark the regions within which each transition was mapped. The horizontal and vertical axes show the R.A. (Δα cos b) and decl. (Δδ) offsets in arcseconds relative to α = 18h56m28.4s, β = +01°29’59” (J2000.0).}\]
based on a simple LTE (local thermodynamic equilibrium) treatment of the H$_2$ excitation, a treatment that is accurate for the lower lying transitions but may be an oversimplification in the case of the highest transitions [S(6) and S(7)]. In a future paper, we will present a refined analysis, including non-LTE effects, together with maps of the various physical parameters derived from the H$_2$ (and, for IC 443C, the HD) maps.

While the H$_2$ S(1)–S(7) lines show a clear morphological similarity to each other, a result that is apparent from inspection of the spectral-line maps and is confirmed by the PCA, the H$_2$ S(0) line is typically more extended than, and in W44 and 3C 391 essentially uncorrelated with, the other H$_2$ rotational lines. The [S i] 25 µm line, by contrast, is always well correlated with the H$_2$ S(1)–S(7) lines, despite the fact that its upper state energy is very similar to that of H$_2$ S(0). These behaviors are demonstrated clearly in Figure 19, which present scatter diagrams showing correlations between [S i] and H$_2$ S(0). Each point in Figure 19 shows the mean intensities within a 5″ × 5″ region. The results shown for W28 are very revealing: while [S i] and H$_2$ S(0) are well correlated in W28 (with a linear correlation coefficient of 0.88), the best-fit linear regression yields a positive $x$-intercept, indicating that there is an extended component of H$_2$ S(0) emission (with typical intensity ~2.5 × 10$^{-2}$ ergs cm$^{-2}$ s$^{-1}$ sr$^{-1}$) that is unassociated with measurable [S i] emission. Figure 19 suggests an explanation as to why [S i] 25 µm and H$_2$ S(0) are reasonably well correlated in IC 433C and W28 but not in W44 and 3C 391; in W28 and IC 443C, the shock-excited contribution dominates the variations in the extended component, whereas in W44 and 3C 391 it does not.

The much lower [S i]/H$_2$ S(0) line ratio in the extended component could indicate a much lower abundance of atomic sulfur or, more likely, a lower gas density, the critical density for the [S i] 25 µm line being much greater than that of the H$_2$ S(0) line (see Fig. 9). The extended H$_2$ S(0) emission in these sources has an intensity comparable to that measured by Falgarone et al. (2005), who observed H$_2$ pure rotational emission along a long sight line within the Galaxy that did not intersect any region of high-mass star formation. Falgarone et al. argued that the observed H$_2$ emission originated in a warm gas component (unassociated with SNRs or regions of star formation) that is present within the cold, quiescent ISM. Alternatively, or in addition, the H$_2$ S(0) emission within SNRs might originate within low-density photodissociation regions (PDRs) that are irradiated and heated by UV radiation from nearby fast shocks. In contrast to the continuum radiation incident on typical PDRs, the UV radiation emitted by fast shocks is dominated by spectral lines. Although detailed calculations will be needed to model PDRs that are irradiated by UV emission from fast shocks, we speculate that a line-dominated spectrum may be particularly effective in exciting H$_2$ rotational emissions, since except for spectral lines that happen to coincide with an H$_2$ Lyman or Werner band transition, line radiation can heat the gas without photodissociating molecules.
It is also noteworthy that the [S\textsc{i}] emission is better correlated with the warm H$_2$ than with the ionized species in these sources. Haas et al. (1991) had previously suggested that [S\textsc{i}] was a tracer of fast dissociative shocks, rather than the slower nondissociative shocks responsible for the H$_2$ emissions. At least in the SNRs that we have mapped with Spitzer, the PCA strongly suggests that [S\textsc{i}] traces slow nondissociative shocks.

The atomic sulfur abundance can be estimated from the [S\textsc{i}] $25\ \mu$m line flux. Unfortunately, the critical density for the [S\textsc{i}] $25\ \mu$m line is probably large in neutral gas ($\sim 10^6\ \text{cm}^{-3}$ according to Table 5 of Hollenbach & McKee [1989]), so the derived S\textsc{i} abundance depends on both the gas density and the adopted rate coefficient for excitation of S\textsc{i} in collisions with H$_2$. IC 443C presents the best case for determining the atomic sulfur abundance, because a measurement of the HD $R(4)/R(3)$ line allows the gas pressure to be determined for this case (Neufeld et al. 2006a). Adopting the H$_2$ column densities and temperatures obtained from a two-component fit to the rotational diagram, assuming the warm and hot gas components to be at a common pressure adjusted to match the HD $R(4)/R(3)$ line ratio (Neufeld et al. 2006a), and making use of the Hollenbach & McKee (1989; hereafter HM89) estimate of the rate coefficient for excitation of [S\textsc{i}] fine-structure collisions, we derive an atomic sulfur abundance of $\sim 10^{-6}$ relative to H$_2$. This value corresponds to $\sim 4\%$ of the solar abundance of sulfur (1.4 $\times$ 10$^{-5}$ relative to H nuclei; Asplund et al. 2005). The uncertainty in this estimate is large, not least because of the absence of a reliable estimate for the excitation rate coefficient. Owing to the presence of a significant UV radiation field produced by fast dissociative shocks in the vicinity of the warm molecular component, Snell et al. (2005) argued that sulfur could be significantly ionized within the nondissociative molecular shocks that are responsible for the pure rotational emissions from H$_2$; thus, the observed S\textsc{i} abundance might be entirely consistent with a negligible depletion of sulfur onto grains and a negligible fraction of the sulfur nuclei being bound within gas-phase molecules. Further discussion of the atomic sulfur abundance, and its implications for the chemistry of interstellar sulfur molecules, is deferred to a future paper.

5.2. Line Emission from Ionized Species

The PCA shows a very tight correlation between the [Fe\textsc{ii}], [P\textsc{ii}], and [Si\textsc{ii}] line intensities in all the regions we observed, a result confirmed by the correlation plots shown in Figures 20 and 21 ([Fe\textsc{ii}] vs. [Si\textsc{ii}] intensity and [P\textsc{ii}] vs. [Si\textsc{ii}] intensity, respectively). These close correlations are unsurprising, given the similar appearance potentials (all $< 13.6\ \text{eV}$) of Fe$^+$, P$^+$, and Si$^+$; all three ions are expected behind shocks that are fast enough to cause significant ionization, and can also be produced in the ionizing "precursors" of fast shocks, where ultraviolet radiation propagates upstream and can photoionize the gas before it even enters...
the shock front. For shocks propagating in molecular gas, the calculations of HM89 suggest that a shock velocity of at least 35 km s\(^{-1}\)/\(C_0\) is required to produce detectable fine-structure emissions from \([\text{Fe}\,\text{ii}]\) and \([\text{Si}\,\text{ii}]\).

One additional feature of the data, however, that is not revealed by our PCA of mean-subtracted line maps is that the correlation plots typically show positive intercepts on the horizontal \([\text{Si}\,\text{ii}]\) axis. As in the case of \(\text{H}_2\), this behavior implies the presence of an extended gas component within which \([\text{Si}\,\text{ii}]\) is enhanced relative to \([\text{Fe}\,\text{ii}]\) and \([\text{P}\,\text{ii}]\).

Four ions of appearance potential greater than 13.6 eV are detected in one or more regions: \(\text{Ne}^+\), \(\text{Ne}^{++}\), \(\text{Fe}^{++}\), and \(\text{S}^{++}\). Such ions, which have been observed widely in SNRs (e.g., Raymond et al. 1997), are produced only in faster shocks. For example, when shocks propagate in molecular gas clouds, velocities \(\gtrsim 80\) km s\(^{-1}\) are needed to ionize Ne (HM89). These lines are generally well-correlated with each other, with the curious exception of the two \([\text{Si}\,\text{ii}]\) lines (19 and 33 \(\mu\)m); in W44, the \([\text{Si}\,\text{ii}]\) lines are anticoordinated with the other emissions from ionized species. We speculate that this behavior could represent an excitation effect, the critical density for the \([\text{Si}\,\text{ii}]\) transitions being smaller than those for \([\text{Ne}\,\text{ii}]\) and \([\text{Ne}\,\text{iii}]\). The \([\text{Si}\,\text{ii}]\) 18.7/33.5 \(\mu\)m and \([\text{Ne}\,\text{ii}]\) 15.6/36.0 \(\mu\)m line ratios both provide useful constraints on the electron density in the emitting region (Alexander et al. 1999). The observed \([\text{Si}\,\text{ii}]\) 18.7/33.5 \(\mu\)m line ratio was 0.78, 0.54, and 0.55, respectively, in W44, W28, and 3C 391, the three sources in which \([\text{Si}\,\text{ii}]\) emissions were detected. All three values are consistent with the low-density limit obtained by Alexander et al. (1999; 0.6 at a temperature of \(10^4\) K or 0.7 at a temperature of \(2 \times 10^4\) K). Conservatively estimating the likely error on the ratio as \(\pm 35\%\), assuming that the gas temperature is at least \(10^4\) K, and making use of the results presented by Alexander et al. (1999; their Fig. 3), we obtain upper limits on the electron density of \(600\), \(200\), and \(200\) cm\(^{-3}\) for W44, W28, and 3C 391, respectively. For all three sources, our best estimate of the \([\text{Si}\,\text{ii}]\) 18.7/33.5 \(\mu\)m line ratio is somewhat smaller than, but probably consistent with, that obtained by Oliva et al. (1999) from ISO observations of the young SNR RCW 103 (0.89 \(\pm 0.18\)). The observed \([\text{Ne}\,\text{ii}]\) 15.6/36.0 \(\mu\)m ratio was \(\sim 11\) in both W28 and 3C 391 (and was consistent with 11 in W44 and IC 443 where the 36.0 \(\mu\)m transition was not detected). Once again, this value is similar to that observed by Oliva et al. (1999) toward RCW 103 (10 \(\pm 2\)), and is consistent with the low-density limit obtained by Alexander et al. (1999; 11 at temperatures of both \(10^4\) K and \(2 \times 10^4\) K), but in this case the implied upper limit on the electron density is \(\sim 10^4\) cm\(^{-3}\) for both W44 and 3C 391. Thus, the observed 18.7/33.5 \(\mu\)m and \([\text{Ne}\,\text{ii}]\) 15.6/36.0 \(\mu\)m line ratios are entirely consistent with a picture in which the \([\text{Si}\,\text{ii}]\) emissions originate in a spatially distinct gas component of lower density than that responsible for the observed \([\text{Ne}\,\text{ii}]\) emissions. In a future paper, we will present a more detailed analysis of the emission from ionized species in these sources, in the context of theoretical models for fast shocks and PDRs.
Fig. 14.—Results of PCA analysis for W44. Top: Fraction of the variance accounted for by each component (asterisks), along with the cumulative fraction for the first \( n \) components as a function of \( n \) (squares). Bottom left: Coefficients for the first and second principal components needed to approximate the maps of each transition. Bottom right: Coefficients for the second and third principal components. Where multiple transitions of a single ion have been observed, the labels distinguish between the different transitions by giving the wavelength rounded to the nearest micron.

Fig. 15.—Same as Fig. 14, but for W28.
Fig. 16.—Same as Fig. 14, but for 3C 391.

Fig. 17.—Same as Fig. 14, but for IC 443C.
6. SUMMARY

We have carried out spectroscopic mapping observations, covering the 5.2–7.0 μm spectral region, toward the supernova remnants W44, W28, IC 443C, and 3C 391, with the use of the Infrared Spectrograph (IRS) of the Spitzer Space Telescope. In each case, a region ~1′ × 1′ has been mapped. Except in 3C 391, which is more distant and has a much smaller angular size than...
the other objects we observed, the mapped regions cover less than 1% of the total radio-emitting area of the SNR.

2. These observations, performed using the short-low, short-high, and long-high modules of the IRS, have led to the detection of a total of 15 fine-structure transitions of Ne++, Ne ++ (two transitions), Si++, P++, S++, S+++ (two transitions), Cl++, Fe++, the S(0)–S(7) pure rotational lines of molecular hydrogen; and the R(3) and R(4) transitions of hydrogen deuteride (reported previously by Neufeld et al. 2006a).

3. We have performed a PCA of the spectral-line maps obtained from our observations, with the goal of characterizing the differences and similarities between the spatial distributions of the various line emissions. In W44 the PCA reveals that the observed emission lines fall into five distinct groups, each of which exhibits a distinct spatial distribution: (1) lines of S and H2(J > 2); (2) the H2(0) line; (3) lines of ions with appearance potentials less than 13.6 eV; (4) lines of ions with appearance potentials greater than 13.6 eV, not including S++; and (5) lines of S++. In the other sources, some of these groups share a common distribution, but in no case do the spectral lines within a group defined above fail to be strongly correlated with each other. This behavior suggests that the line emissions we have observed originate in at least five physically distinct components (some of which have similar distributions, as projected onto the sky, in sources other than W44).

4. The observed lines of S and H2(J > 2) likely originate in molecular material subject to a slow, nondissociative shock that is driven by the overpressure within the SNR. For the case of IC 443C, where the gas pressure is constrained by the HD R(4)/R(3) ratio (Neufeld et al. 2006a), we estimate the atomic sulfur abundance as ≈10−6 relative to H2 (with a large uncertainty), a value corresponding to ≈4% of the solar abundance of sulfur. Given the possible presence of S+ in the [S i] emitting-region, this observed atomic sulfur abundance might be entirely consistent with a negligible depletion of sulfur onto grains and a negligible fraction of the sulfur nuclei being bound within gas-phase molecules.

5. The H2S(0) line is typically more extended than any of the other spectral lines we have observed. In W28 it shows clear evidence for both a shock-excited component and a low-density diffuse emission component.

6. The fine-structure emissions from singly and doubly charged ions originate primarily in dissociative shock fronts with a range of shock velocities. Those ions with appearance potentials greater than 13.6 eV originate in faster shocks than, and show a different distribution from, ions with appearance potentials less than 13.6 eV. In W44 the S++ emissions show a very different distribution from those of other ions of similar appearance potential (e.g., Ne++), a behavior which may reflect the lower critical density for the observed S++ emission lines.

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