Axion-photon multimessenger astronomy with giant flares

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We treat prospects for multimessenger astronomy with giant flares (GFs), a rare transient event featured by magnetars that can be as luminous as a hundred of the brightest supernovae ever observed. The beamed photons could correlate with an axion counterpart via resonant conversion in the magnetosphere. In a realistic parameter space, we find that the sensitivity limit to galactic GFs for currently viable experiments is \( g_{\phi\gamma} \gtrsim \text{several} \times 10^{-13} \) GeV\(^{-1}\) \& \( g_{\phi\gamma} \gtrsim \text{few} \times 10^{-12} \). We rule out the compatibility of axion flares with the recent XENON1T excess only due to the time persistence of the signal.

I. BACKGROUND

The Quantum Chromodynamics (QCD) axion \([1,2]\) is a hypothetical pseudo-scalar boson that arises from the strong interaction \([3]\). The axion mass — dynamic solution to the charge and parity (CP) problem — can be several orders of magnitude below the QCD scale. The coupling constants — \( g \) — are unknown in spite of the remarkable effort realized to find axion in the parameter space at which that can simultaneously solve the CP problem and the dark matter (DM) enigma \([4,7]\).

Relevant interactions of axion-like particles to Standard Model (SM) particles for this work are

\[
\mathcal{L}^{\text{int}} = -\frac{1}{4} g_{\phi\gamma} F_{\mu
u} \tilde{F}^{\mu\nu}\phi + i g_{\phi\gamma} \bar{\psi} \gamma^\phi \psi, \tag{1}
\]

where the first term on the right-hand side represents the effective axion-photon Lagrangian density and the second term the axion-electron coupling: being \( \phi \) the axion field, \( F^{\mu\nu} \) the photon field, \( \psi \) the electron field and \( \gamma^\phi \) the usual matrix.

II. AXION-PHOTON MIXING IN ASTROPHYSICAL ENVIRONMENTS

A. General dispersion relations

Aided by axion-electrodynamics \([8]\) for the linearization of the equations of motion from Eq.\([1]\) a set of Schrödinger-like dispersion relations emerges that can be solved analytically in idealized astrophysical boundaries \([9] \& [10]\):

\[
\begin{bmatrix}
\omega + \Delta_1 + \Delta_{Q1} \\
\Delta_R \\
\Delta_{M1}
\end{bmatrix}
\begin{bmatrix}
\Delta_R \\
\Delta_p + \Delta_1 + \Delta_{Q1} \\
\Delta_{M1}
\end{bmatrix}
\begin{bmatrix}
\Delta_{M1} \\
\Delta_{M2} \\
\Delta_{Q2}
\end{bmatrix}
-i \partial z \begin{bmatrix}
\bar{E}_1 \\
\bar{E}_2 \\
\bar{E}_3
\end{bmatrix} = 0. \tag{2}
\]

The interaction term \( \mathcal{L}^{\phi\gamma} = g_{\phi\gamma} E \cdot B \) is obtained from Eq.\([1]\) being \( E \) the photon and \( B \) the external magnetic field, establishing a preferential polarization. Now, obviating the Faraday rotation term — \( \Delta_R \) — the perpendicular component \( E_\perp \) decouples and the mixing is reduced to a 2D system given by the low-right sector in the second term of the left-hand side of Eq.\([2]\). The term \( \Delta_R = \frac{1}{2} \Delta_{\|} \left( n_e - 1 \right) \) vanishes in the weak dispersion limit, since the refraction index is \( n_e \sim 1 \) for relativistic axions.

The quantum-electrodynamics (QED) vacuum refraction parameter — \( \Delta_Q \) — can be treated independently. We have defined the refraction parameter \( \Delta_p = -\omega_p^2/2\omega \), with \( \omega_p = (e^2 n_e/m_e c_0)^{1/2} \) the characteristic frequency of the plasma, and the axion mass parameter \( \Delta_\phi = -\mu^2_{p}/2\omega \). The coupling term is \( \Delta_M = g_{\phi\gamma} B/2 \). We also define \( \Delta k^2 = (\Delta_p + \Delta_\phi - \Delta_{Q1})^2 + 4\Delta_M^2 \) and the mixing angle that holds the diagonalization, \( \tan(2\theta_m) = 2\Delta_M/(\Delta_p - \Delta_\phi) \).

B. The role of the plasma density in the relative weight of QED corrections

It has been pointed out that QED vacuum polarization effect acts as a suppressor of the axion-(keV)photon cross-section in a minimal model of neutron star adopting the Goldreich-Julian (GJ) corotation density — \( n_{\text{GJ}} = 4\pi r^2 B(r) (eP)^{-1} \). However, a pair multiplicity factor, defined \( \kappa = n_e/n_{\text{GJ}} \), emerges in modern approaches beyond the GJ paradigm \([11]\). The ratio of plasma effects to QED vacuum effects, manifest through the Euler-Heisenberg term \( \mathcal{E}_{\text{QED}} = \frac{\alpha^2}{96\pi^2} \left[ (F_{\mu\nu} F^{\mu\nu})^2 + \frac{\tau}{4} (F_{\mu\nu} \tilde{F}^{\mu\nu})^2 \right] \), scales with the density profile across the gas \([11,12]\):

\[
\frac{\Delta_p}{\Delta_{Q1}} = 5 \times 10^{-10} \left( \frac{\text{keV}^2 \times 10^8 [\text{T}] \text{1[s]}}{B(r) \frac{\text{[T]}}{\text{P}}} \right) \kappa. \tag{3}
\]

From Eq.\([3]\) it follows that the tension with QED results progressively relaxed above \( \kappa \gtrsim 10^5 \) at relatively large distances from the star for keV photons, while \( \Delta_Q \) gradually vanishes near its surface for \( \kappa \gtrsim 10^6 \). In the case of very energetic transitory events featured by magnetars, the charge density near the star surface is \( n_e \sim 10^{30}\text{cm}^{-3} \).
many orders over the occupation number predicted by the GJ model. Although the density profile through the atmosphere of the ‘fireball’ is barely known, simulations suggest that pair multiplicity factors $\kappa \lesssim 10^{10}$ are tenable at an altitude of few stellar radii \[13\]. That renders resonant conversion efficient in the parameter space dominated by plasma effects; including highly magnetic neutron stars, where $10^{4−5} \lesssim \kappa \lesssim 10^{7}$ \[11\] \[15\], against previous expectations.

C. Magnetar axion

Magnetars are compact stellar remnants endowed with extreme magnetic fields, typically about $10^{10−11}$ T, a ‘canonical’ mass around 10-20 solar masses and a rotation period of the order of seconds \[10\]. In the standard picture, their persistent emission mechanisms involve pair production and magnetic acceleration, catalyzing the migration of charges to higher altitudes from the star to give rise to curvature radiation, synchrotron emission and inverse Compton scattering \[14\] \[15\]. The beamed photons could be converted to axion through non-adiabatic resonant mechanism at their path across the non-relativistic, ‘cold’, plasma of the magnetosphere \[11\] \[12\] \[19\] \[22\]. In the aligned-rotator approximation, where the magnetic axis and the rotation axis — $\hat{z}$ — are superimposed, the axion-photon oscillation amplitude is derived from introducing the resonance condition $\Delta_p - \Delta_\phi = 0$ in Eq.2 yielding a conversion probability $P_{\gamma\phi} = \Delta^2 k / (2 \partial \Delta_p)$. Since outgoing photons present a gradient $\partial \Delta_p \sim m_\phi^2 \omega^{-1} z_c^{-1}$, it is straightforward to obtain \[11\]

$$P_{\gamma\phi} = \frac{g_\phi^2 B^2(z_c) \omega z_c}{m_\phi^2}.$$ \hspace{0.5cm} (4)

In Eq.4 $B(r) = B_0 (R/r)^3$ expresses the magnetic field in the dipole approximation, stationary as a result from an aligned rotator, as a function of the distance from the surface of the star, $z_c$ is the conversion altitude, $\omega$ the pulse of the photon.

III. MAGNETAR FLARES AND THEIR AXION COUNTERPART

A. Magnetar flares

The so-called anomalous X-ray pulsars (AXPs) and soft gamma-ray repeaters (SGRs) today are thought to be transient events from magnetars. Their strong outbursts are frequently referred short-bursts (SBs), intermediate flares (IFs) and giant flares (GFs), whose more general characteristics are summarized in Table I. If the quiescent emission mechanisms of magnetars are poorly understood, the scenario for transient events is even more complex. Rapid magnetic field reconfiguration is thought to be an important part of the outbursts. The released magnetic energy is converted then to thermal energy in the magnetosphere — cf. \[23\] for solved non-thermal spectral features —. However, the triggering mechanisms, and the exact role of the magnetic field remain unresolved. The time-scale of the magnetic reconnection — $t_{\text{rec}} \sim L/V$, where $L$ is the height of the reconnection point and $V$ the inflow velocity — should be much larger than the typical time-scale of the system, $\tau \sim \omega^{-1} m_\phi^{-1}$, to render plausible the conversion mechanism described by Eq.4. Within this scenario, reasonable for a relatively high frequency or a sufficiently high distance from the star, we have $\tau < t_{\text{rec}}$ and the oscillation takes place in a pseudo-stationary regime. We include the spectra of an IF with energy-scale about $10^{41}$ erg s$^{-1}$ in Fig.\[1\] left. The correlated axion flare is quantified in units of the typical occupation of virialized dark matter in the Galactic halo, around $10^{13}$ keV cm$^{-2}$ s$^{-1}$.

We will confine our attention throughout the following sections to the study of axion giant flares (AGFs) triggered by GFs. Three ‘galactic’ GFs have been observed: from SGR 0526-66, actually hosted by Large Magellanic Cloud (LMC), in 1979 \[25\], from SGR 1900+14 in 1998 \[26\] and, the most luminous to date, from SGR 1806-20 in 2004 \[24\] \[27\] \[28\]. Although there is consensus that GFs are rare events, the exact rate is source of controversy and is susceptible to observational bias \[29\]. Statistics in \[30\] suggests that the rate for events above $10^{44}$ erg is $\sim 3.8 \times 10^{5}$ Gpc$^{-3}$ yr$^{-1}$, resulting in a event rate per magnetar of the order of $\lesssim 0.02$ yr$^{-1}$. These estimates rely on the strong evidence that 1-20% of the gamma-ray burst (GRB) sample are indeed extragalactic GFs, whose tails are undetectable due to the large distance \[13\]. In that manner, the catalogue of confirmed GFs is poor and, in addition, their spectral features are not adequately characterized due to saturation of the detectors and other systematics. Therefore, we fit and extend to low frequency a black-body (BB) curve at a temperature $k_B T_{\text{BB}} \sim 175$ keV, with a fluence of $1.36 \times 10^{-3}$ erg cm$^{-2}$ of $>30$ keV photons on Earth consistent with the SGR 1806-20 event \[27\], to be employed in simulations throughout the following sections. Notwithstanding that empirical data are not available when referring to the polarization of

| Feature | Object | Time-scale [s] | $\nu$ [erg s$^{-1}$] |
|---------|--------|---------------|----------------|
| Quiescent | Magnetar | - | $1.10^{43}$ |
| SB | AXP&SGR | 0.2–1 | $1.10^{41}$–$10^{44}$ |
| IF | AXP&SGR | 1–40 | $1.10^{41}$–$10^{44}$ |
| GF | SGR | $<0.5+\text{tail}$ | $1.10^{44}$–$10^{47}$ |

\[a\] Duration of the peak.  
\[b\] Bolometric luminosity; isotropic flux.  
\[c\] Typical value with a variability of several orders of magnitude.  
\[d\] A few-hundred seconds scattering tail with a lower luminosity follows the main peak.
resulting in the well-known expression \[\text{[38]}\] relations, or form of a thin disk of after consulting the literature \[\text{[31–34]}\]. The weight of modes, i.e., ordinary (O) — with the E field lying on the k-B plane — and extraordinary (X). The weight of magnetars linearly polarizes the photons in two normal dimensions. We adopt QCD axion coupling strength. The non-adiabatic resonant model is ruled out in sectors where O-modes become evanescent, or equivalently \(\omega_p > \omega\); \(\Gamma > 1\) regions, being \(\Gamma\) the adiabaticity factor of the system; ‘weak-field’ zones, with \(\omega \gtrsim \omega_p\), being \(\omega_p = eB(z_c)/m_e\) the gyrofrequency; sectors where QED vacuum polarization effect governs the dispersion relations, or \(\Delta_p < \Delta_Q\). In a consequence, axions with \(m_\phi \gtrsim 10^{-7} \text{ eV}\) mix efficiently with 1-10 keV photons.

B. The flight of axion to Earth

Obviously, both the photon and axion flux suffer from the inverse-square law with distance. Moreover, axions with a rest mass \(m_\phi \lesssim 10^{-5} \text{ eV}\) crossing through several cosmic magnetic domains, with a typical length scale — \(s\) — of the order of Mpc, are reconverted efficiently into photons; first across their outgoing path through the intergalactic medium (IGM), and then upon reaching the Milky Way (MW) \[\text{[35–37]}\]. The photon-to-axion conversion probability, derived from Eq.3 is read \(P_\phi = 4\Delta^2 M \sin^2(\ell\Delta k/2)/\Delta^2 k\). In the strong-coupling limit, the inequality \((\Delta_p + \Delta_Q - \Delta_\phi)^2 \ll 4\Delta^2 M\) is obtained, resulting in the well-known expression \[\text{[38]}\]

\[
P_\gamma = \frac{g^2_{\phi\gamma} B^2 \ell^2}{4}. \tag{5}\]

From a panoramic perspective, our galaxy takes the form of a thin disk of \(~30\) kpc length — i.e., \(\ell \ll s\) — with a magnetic field of the order of a fraction of nT, and a low electron density, about \(10^{-3} \text{ cm}^{-3}\). Crucially, from Eq.5 it follows that only a marginal fraction of the magnetar axions released in the vicinity of the MW are reconverted into photons during their approximation to Earth. In other words, the astroparticle flux density at origin, determined by Eq.4 approximately persists.

Photons are massless through the IGM. Axion is massive. In contrast to the plasma that envelopes the magnetosphere, where the resonant conversion takes place at \(\omega_p \sim m_\phi\), the relation \(\hbar \omega \sim \gamma m_\phi\) is maintained through the vacuum, being \(\gamma\) the Lorentz factor. The axion velocity is \(\beta_\phi = \sqrt{1 - 1/\gamma^2}\). In that form, the delay time, at keV energies, for values of the Lorentz factor between \(10^3\) and \(10^8\) varies between about a year per traveled kpc and a few milliseconds. That would render photon-axion multimessenger astronomy constrained to a human-scale time frame and would motivate the tracking of confirmed outbursts for relatively massive axions.

IV. OBSERVABLE EFFECTS

A. Detection of axion flares through inverse Primakoff-effect

The solar axion spectra is formed by interactions of axion with SM particles in the internal plasma of the star. A spectra dominated by Primakoff-effect presents a maximal flux about \(10^9 \text{ cm}^{-2} \text{s}^{-1}\) at 3-4 keV for an axion-photon coupling strength \(g_{\phi\gamma} \sim 10^{-11} \text{ GeV}^{-1}\). A solar spectra shaped by atomic recombination and deexcitation, bremsstrahlung, and Compton (ABC) processes peaks a similar fluence around 1 keV for an axion-electron...
coupling strength is approximately $g$. Sensitivity of helioscopes in terms of the axion-photon coupling is set by Eq.\ref{eq:4}. Helioscopes are directional detectors tracking the Sun and a high homogeneity, overlapping other model-dependent, or indirect, results \cite{55–57,61,62}. Dark lines correspond with direct detection of giant flares with 15 — dotted —, 3 — dashed — and 0.1 — solid — kpc distance, at 95% CL. The comparison is performed by integration of the spectral functions between 1-10 keV, where the detectors are more sensitive coinciding with the maximal flux of solar axion.

FIG. 2. Limit on the sensitivity to axion flares by realistic helioscope-like detectors, based on the inverse Primakoff-effect. The CAST helioscope limit is established at 95% confidence level (CL) \cite{39}. The horizontal branch (HB) exclusion region is established by indirect methods at 95% CL \cite{40}. Astro-bounds established by indirect methods are also included in green \cite{41,42}. The light brown solid line represents the KSZV axion. The dot-dash yellow line projects new-generation helioscope sensitivity at 95% CL from a campaign lasting several years \cite{43}, while the duration of the giant flare is set $t=0.125$ s. Dark lines correspond to direct detection of GFs with 15 — dotted —, 3 — dashed — and 0.1 — solid — kpc distance, at 95% CL. The comparison is performed by integration of the spectral functions between 1-10 keV, where the detectors are more sensitive coinciding with the maximal flux of solar axion.

Helioscopes are directional detectors tracking the Sun and magnetar scanning performed by an IAXO-like instrument \cite{43,43}. There, we find a volume of special interest in a $\lesssim$3 kpc radius from Earth, with around three dozen cataloged magnetars, being about $1/3$ of them within a $1/2$ kpc radius; while the closest object is about 0.1 kpc distant \cite{54}.

B. Observation of axion flares using liquid-xenon detectors

Experiments storing liquid-xenon are sensitive to axion through the axio-electric effect — $\phi + e + Z \rightarrow e' + Z$ — hold by Eq.\ref{eq:1}. In the relativistic limit, the cross-section reads

$$\sigma_{\text{pe}}[\text{cm}^2\text{kg}^{-1}] \simeq 10^2 \times g_{\phi e}^2 \left(\frac{E}{\text{keV}}\right)^2 \left(\frac{\sigma_{\text{pe}}(E)}{10^9 \text{ b}\text{atom}^{-1}}\right), \quad (7)$$

where the proton-electron cross-section $\sigma_{\text{pe}}(E)$ can be, e.g., interpolated from \cite{63}. By the introduction of an expectation signal-to-noise ratio (SNR) in Eq.\ref{eq:7} it is possible to write the sensitivity of liquid-xenon detectors in terms of the axion-electron coupling strength \cite{64}

\[
g_{\phi e} \simeq 10^{-13}. \text{ Differently from magnetar axion, one finds from Eq.\ref{eq:1} that the QCD axion flux is enhanced for X-ray photons, the emitted solar flux scales with } g^2 \text{ mitigating the emission of axion-like particles (ALPs) with a low coupling strength, including both KSZV and DFSZ axion.} \\

\text{Helioscopes are directional detectors tracking the Sun and a high homogeneity, overlapping other model-dependent, or indirect, results \cite{55–57,61,62}. Dark lines correspond with direct detection of giant flares with 15 — dotted —, 3 — dashed — and 0.1 — solid — kpc distance, at 95% CL. The comparison is performed by integration of the spectral functions between 1-10 keV, where the detectors are more sensitive coinciding with the maximal flux of solar axion.}

耦合常数 $g_{\phi e} \simeq 10^{-13}$。不同地用磁体，用一个从$\phi + e + Z \rightarrow e' + Z$ — 被$g_{\phi e}$等式所约束的QCD axion flux是X射线光子增强的，射出的日光量子是$g^2$抑制的。用低耦合强度的粒子（ALPs）与低耦合的KSVZ和DFSZ axion

超导液-氦探测器是沿着太阳和磁体扫描的探测装置。其工作原理是利用逆普里马科夫自光-光转换，其中$\phi$和$\gamma$在磁性冷气室中，配以光电倍增管（PMTs）。跨距超过10 kV，其中的探测器是更敏感的，与光子-光子转换的最大化相一致。

FIG. 3. Limit on the sensitivity to axion giant flares (AGFs) based on the axio-electric effect for realistic liquid-xenon detectors. The regions shaded in warm colors are established by direct detection of solar axion at 90% confidence level (CL) \cite{55–57,60}. The light reddish zone corresponds with methods whose hypothesis that all the dark matter in the Halo is formed of axion and a high homogeneity, overlapping other model-dependent, or indirect, results \cite{55–57,61,62}. Dark lines correspond with direct detection of giant flares with 15 — dotted —, 3 — dashed — and 0.1 — solid — kpc distance, at 95% CL. The red solid line corresponds with DFSZ, non-relativistic, axion. Parameters are $t = 0.125$ s, $W = 10^4$ kg, $R = 0.3137 \sqrt{\text{keV}}$, $b = 1.4 \times 10^{-5}$ s$^{-1}$ kg$^{-1}$ keV$^{-1}$.
cles with an axion-photon coupling provide the detectors with sensitivity to axion-like particles. We find that GFs originating in the vicinity of Earth would be calibrated against data from X-ray telescopes and grounded by theory. The expected axion flux density on Earth results from the convolution of three terms: the GF photon spectral flux density, the photon-to-axion conversion probability and the geometric dilution with distance. As a reference, for an upper-limit photon-axion conversion probability $O(1/2)$, the flare from SGR 1806-20 — $10^{46}$ erg, 15 kpc distance — would result in a transient fluence on Earth similar to the flux of solar axions for an axion-photon coupling strength $g_{\phi \gamma} \approx 10^{-11}$ GeV$^{-1}$.

Assuming axion, this work predicts the existence of axion giant flares (AGFs) across our universe, and perhaps their detectability by ground-based observatories. Transcendentally, the echo of a galactic flare might be received today in the form of AGF, due to the delay-time that massive particles suffer compared to ordinary photons during their flight through the interstellar medium. Thus, monitoring the confirmed sources of giant flares — SGR 0526-66, 48 kpc distant, in 1979; SGR 1900+14, 6 kpc distant, in 1998; and SGR 1806-20 in 2004 — with dark matter detectors, in addition to future events, can be motivated — e.g., during hours when helioscopes cannot track the Sun. A state-of-the-art estimate of the event rate suggests that each magnetar releases up to one poten giant flare every fifty years. There are currently more than four dozen cataloged magnetars within a radius of 15 kpc from Earth. Therefore, the probability of an observable AGF event would be in the order of a dozen in the next decade, with approximately 2/3 of them originating within a distance of 3 kpc. In addition, it is striking that, although the bursts themselves are not periodic, the activity might only occur during predictable periodic intervals. As a consequence, the prediction and tracking of magnetars entering an active period using dedicated axio-telescopes, or a network, is not discardable in order to enhance the probability of detection through the observation of stars with active, non-overlapping windows.

Finally, the XENON1T Collaboration recently reported an electronic recoil excess below 7 keV compatible with solar axion at 3.4$\sigma$ CL. However, the precise parameter space is in tension with stellar evolution at 8$\sigma$. Interestingly, magnetar axions could mimic solar axion at keV energies without conflicting with stellar physics. However, the signal persisted for a large time interval incompatible with the known nature of magnetar flares, while quiescent isolated sources would be too distant to provide the deposited energy. Magnetar axion count rate could be a factor to consider in future experiments.

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