Theoretical study of metal-free catalytic for catalyzing CO-oxidation with a synergistic effect on P and N co-doped graphene

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P and N co-doped graphene (PN_xC_y-G with x = 1, 2, 3 and y = 0, 1, 2) is designed to enhance graphene reactivity with a synergistic effect of the P and N atoms for the CO oxidation reaction, focusing on the influence of the N dopant concentration on graphene. The calculated results indicate that increasing two or three coordinated N to P can facilitate charge transfer from the surface onto O_2 molecules. However, the adsorbed O_2 molecule breaks apart on PN_3-G surface, affecting CO oxidation performance. Furthermore, PN_2C_1-G exhibits excellent catalytic activity towards the oxidation of CO via the ER mechanism, which catalyzes CO oxidation with the rate-determining step of only 0.26 eV for the first and 0.25 eV for the second oxidation at 0 K. Additionally, the catalytic oxidation of PN_2C_1-G via Eley–Rideal mechanism prefers to occur at room temperature (298.15 K), with a rate-determining step of 0.77 eV. The reaction rates at 298.15 K is calculated to be 5.36 × 10^{16} mol s^{-1}. The rate constants are obtained according to harmonic transition state theory, which could be supportive for catalytic oxidation of CO on the experiment.

Carbon monoxide (CO) is a well-known air pollutant. Generally, CO gas occurs from the combustion processes of industry, factories, and incomplete combustion by gasoline and diesel-fueled engines. Importantly, it causes dangerous effects when we breathe CO which is harmful to the heart and brain. Therefore, removing this toxic gas are essential for environmental safety. The conversion of CO to carbon dioxide (CO_2) is a desirable method in heterogeneous catalysis. Although CO_2 is a greenhouse gas responsible for global warming, it is not hazardous to human health.

The catalytic oxidation of CO has been studied to find an efficient catalyst to control the pollutant. The CO oxidation reaction route involves the direct oxidation of CO to CO_2 by oxygen (O_2) adsorbed on the surface of a catalyst. Previously, various noble metals, such as Pt, Pd, Cu, Fe, Rh, and Au were investigated for the development of a catalyst for CO oxidation. Such catalysts are highly active toward the oxidation of CO; however, noble metals are rare and expensive. Moreover, these metal catalysts usually operate at a high reaction temperature. Thus, it is of great interest to develop efficient and low-cost catalysts for the low-temperature operation of the CO oxidation reaction. Metal-free catalysts have attracted attention due to their high activities in the catalytic oxidation reaction.

Various kinds of carbon-based materials, such as carbon nanotubes and graphene, have been studied to search for a metal-free catalyst for the oxidation of CO. Graphene is interesting material because of its unique properties deriving from a two-dimensional layered structure of sp^2-hybridized carbon. Using sp^2-hybridized carbon atoms to form hexagons is the focus of intensive investigation due to their significant physical and chemical properties. In particular, the high surface area, high chemical stability, and outstanding conductivity of graphene make it an
ideal support for metal atoms and clusters in making novel carbon–metal nanocomposite catalysts\textsuperscript{8–12}. Besides, vacancy defects on graphene could enhance the binding and dispersion of both metals and metal-free catalysts. Recent studies have shown that the doping with heteroatoms on defective graphene effectively modifies its characteristics and improves stability in catalytic applications. As a result of comparing supported metal and non-metal catalysts, the supporting metals indicate their practical and high activity attributes due to the strong interaction between metals. The supporting substrate modify the charge redistribution and affects the reactive performance of the catalyst\textsuperscript{13}. However, the high surface free-energy of metals promotes the formation of the metals into large clusters, and these aggregations affect the catalytic efficiency of a catalyst\textsuperscript{14,15}. Therefore, the substitutional doping of metal-free atoms in the graphene surface is important to adapt the electronic distribution of the graphene system and promote catalyst performance. Additionally, chemically modified graphenes featuring metal-free substituents such as B, N, S and P\textsuperscript{16–18} were reported. The incorporation of a non-metal heteroatom into the graphene lattice is especially a promising approach to improve catalytic activity further. Particularly, N-doped graphene has been attracting considerable attention in theoretical and experimental studies. N-doped graphene is a non-precious metal catalyst for oxygen reduction reactions (ORRs). Additional electrons are introduced into graphene, conferring novel electronic properties by N-doping. Previously, Chang et al.\textsuperscript{19} demonstrated that B-N and P-N co-doped graphenes exhibited greater catalytic activity to reduce O\textsubscript{2} than singly doped N-graphene. In addition, doping by B and P in graphene considerably modifies the electrophysical character of graphene due to the significant electronegativity difference between the B and N atom or P and N atoms, and this difference induces heterogeneity in the graphene surface. Liang et al.\textsuperscript{20} has also reported that P and N co-doped graphene improves the catalytic ability to reduce O\textsubscript{2} due to a synergistic effect, compared to single doping. To the best of our knowledge, no experimental or theoretical study reports are published on the catalytic CO oxidation reaction over P and N co-doped on single vacancy P-embedded graphene. However, P and N doped graphene was synthesized and applied to ORRs. This co-doping strategy will allow graphene based metal-free catalysis being effective in the CO oxidation reaction. The focus of this study is to examine the synergic effect of doped P and N atoms for oxidation of CO by O\textsubscript{2} and to reveal how incorporating an N atom around P can improve the catalytic activity of the surface, the adsorption configuration, and the electronic structure over P and N co-doped graphene. The effect of N dopant concentration on single vacancy P-embedded graphene for the reaction of CO oxidation. Furthermore, all possible reaction pathways for CO oxidation reaction are investigated via density functional theory (DFT).

**Computational details.**

Calculations were performed using the DMol\textsuperscript{3} software package in Materials Studio 7.0\textsuperscript{21} with the Perdew–Burke–Ernzerhof (PBE)\textsuperscript{22} functional in the generalized gradient approximation (GGA). The wave function for all atoms was described in terms of a double numerical basis set with polarization (DNP)\textsuperscript{23}. We used the DFT + D method within the Grimme’s scheme\textsuperscript{24,25} to consider the Van der Waals effects. No symmetry constraint was employed during the geometry optimizations. All geometry optimizations were performed using a convergence tolerance of 1.0 × 10\textsuperscript{−5} Ha, a maximum force of 0.001 Ha/Å, and a maximum displacement of 0.005 Å. To achieve accurate electronic convergence, a smearing of 0.005 Ha and a basis-set cut-off of 4.2 Å were employed.

A 5 × 5 supercell of graphene (containing 50 C atoms) was built as a base material. The vacuum space of 20 Å was set in the z-direction to avoid interactions between periodic images. The Brillouin zone (BZ) integration was sampled using a 5 × 5 × 1 k point. The transition state (TS) of CO oxidation reactions was searched using a linear synchronous transit (LST)/quadratic synchronous transit (QST) method to find the minimum-energy pathway (MEP) for each reaction step. TS optimization computations confirmed the connections of reactant and product to the TS. In addition, the TS was verified by vibrational frequencies, which guaranteed only one imaginary frequency throughout the potential energy surface. The density of states (DOS) was carried out with a k-point grid of 15 × 15 × 1. To further ensure the stability of the catalyst, the molecular dynamics (MD) simulation of PN\textsubscript{x}C\textsubscript{y}-G was carried out for 2.0 ps in the NVT ensemble, with a 2.0 fs time step at 300 K. The Nosé-Hoover chain method\textsuperscript{26} was used to calculate the thermodynamic stability. The following formula was used to obtain the formation energy (E\textsubscript{f}) of PN\textsubscript{x}C\textsubscript{y}-G:

\[
E_f = (E_{PNxCy-G} - \mu_P - n\mu_N + m\mu_C) - E_G
\]  

where E\textsubscript{PNxCy-G} is the total energy of the graphitic PN\textsubscript{x}C\textsubscript{y}-G sheet, and E\textsubscript{G} is the total energy of the pristine graphene. The \(\mu_P\), \(\mu_N\), and \(\mu_C\) are the chemical potentials of P, N, and C atoms, respectively. The x and y parameters are the number of N and C atoms on the graphene sheet. The interaction between gas molecule and surface was studied by calculating the adsorption energy (E\textsubscript{ads}), which is defined by Eq. (2):

\[
E_{ads} = E_{adsorbate/catalyst} - E_{catalyst} - E_{adsorbate}
\]  

where E\textsubscript{adsorbate/catalyst} is the total energy of the adsorbate–catalyst system, E\textsubscript{catalyst} the energy of the optimized PN\textsubscript{x}C\textsubscript{y}-G surface, and E\textsubscript{adsorbate} the energy of a free atom. By this definition, a negative E\textsubscript{ads} value represents an exothermic adsorption.

Next, the reaction rate constants of reaction step were carried out. The microkinetic simulation of the best CO oxidation reaction pathways were performed by using the MKMCXX software package\textsuperscript{27}. The rate constants for the forward and backward elementary reaction were calculated by the Eyring equation:

\[
k = Aexp \left( \frac{-E_a}{k_B T} \right)
\]
where $E_a$, $k$, $k_b$, and $T$ are activation barrier, the reaction rate constant, Boltzman constant and temperature in Kelvin, respectively. Here, the pre-factor $A$ of the Eyring equation can be determined by

$$A = \frac{k_B T Q_{TS}}{h}$$

where $h$, $Q_{TS}$ and $Q$ are the Planck constant, the transition state partition fiction and the initial state partition fiction, respectively. The partition fiction concluded all possible states, inclusive translation, rotation and vibration modes. In this study, the pre-factor $A$ was set to be $10^{13}$ s$^{-1}$ for the elementary surface reactions due to the negligible changes in entropy.

The non-activated molecular adsorption, gas-phase pressure was set to be 1 atm and the gas includes O$_2$, CO and CO$_2$. The gas surface and desorption rates were depicted by the Hertz–Kunden equation.

Thus, the gas adsorption rates constant ($K_{ads}$) and desorption rates constant ($K_{des}$) were provided by following,

$$F = S \frac{P}{\sqrt{2\pi mk_bT}}$$

and

$$K_{ads} = S \frac{PA}{\sqrt{2\pi mk_bT}}$$

where $A$, $m$, $\sigma$, $Q_{rot}$, $S$ and $P$ indicate the area of surface site of adsorption, the mass of molecule, the symmetry number, the characteristic temperature for the rotation, the sticking coefficient (assumed as 1), Three rotational degrees of freedom and two translational degrees of freedom of transition state were assumed for desorption.

**Results and discussion**

**Properties and stability of PN$_x$C$_y$-G graphene sheets.** We first optimized the structure of N doped on single vacancy P-embedded graphene (PN$_x$C$_y$-G). Figure 1 shows the optimized structure of PN$_x$C$_y$-G sheets where $x$ and $y = 0, 1, 2$, and $3$. The calculated atomic charge on the P atom and the formation energy of each graphitic sheet are summarized in supplementary Table 1. The calculated results show that after optimization, the structure of N and P co-doped in PN$_x$C$_y$-G is displaced outward from the graphene surface because of the larger atomic radius of P compared to C and N atoms. The bond distances between P and N in PN$_x$C$_y$-G, PN$_x$C$_{1-y}$-G, and PN$_y$-G sheets are about 1.77, 1.79, and 1.79 Å, respectively, which are slightly longer than the P–C bond in the P–G graphene sheet (1.77 Å). The formation energies for PN$_x$C$_{2-y}$-G, PN$_x$C$_{1-y}$-G, and PN$_y$-G are calculated as $-1.90$, $-1.06$, and $-0.74$, respectively. The result shows that the formation energy of PN$_x$C$_{2-y}$-G is the most negative. Therefore, co-doping of P and one N atom is more energetically favorable for P and N doping on a graphene surface.

Moreover, we also considered the stability of PN$_x$C$_{2-y}$-G, which is also associated with its electron distribution. As shown in Fig. 2, the highest occupied molecular orbital (HOMO) displays differences in electronegativity between P, N, and C atoms, resulting in a local redistribution of charge density and electron aggregation on the highly electronegative N atoms. The blue and yellow in the deformed electron density map illustrate the capture and
release of electrons, respectively. It is clearly seen that HOMOs are mainly distributed on P, N and C, implying that the surfaces are promoted by N atom. Due to the charges of the P and C atoms with weaker electronegativities are also affected by the size of the vacancy. In contrast, the electron densities of HOMO are redistributed for PC3-G, in which a single vacancy P is embedded graphene (Fig. 2a, left). According to supplementary Table 1, a P atom exhibits positive charges in PC3-G (0.638 |e|), PN1C2-G (0.692 |e|), PN2C1-G (0.810 |e|), and PN3-G (0.903 |e|) due to the transferring electrons that move from the P atom to neighboring atoms. Therefore, this charge causes P atom to form covalent bonds with coordinated C and N atoms. Additionally, partial density of states (PDOS) also supports strong interaction of C, N and P atoms on graphene surface (Supplementary Fig. 1). The results indicate that P atom and neighborhood atoms show the strong hybridization between P-3p and neighborhood atoms 2p-orbitals.

To gain deeper insights into the electronic structure of surfaces, we further calculated their density of states (DOS) and band structures. The results of the DOS plots reveal that the addition of a N atom to PC3-G leads to DOS near the Fermi level for PN1C2-G (Fig. 2b, right) whose valence band is close to Fermi level, indicating semi-metallic behavior. As showing in Fig. S2b, the valence band of PN1C2-G slightly shifts down from Fermi level. For PC3-G with 2 and 3 N-coordinations (Fig. 2c, d, right), the band structures, the conduction band clearly shifts down to Fermi level. Thus, amount of coordinated N atom on graphene surface affect to electronic properties of surface. The PN1C2-G surface, doping N atoms impact holes (acceptor states), whereas for the PN2C1-G and PN3-G surfaces, doping N atoms affect electrons (donor states). Therefore, PN1C2-G and PN2C1-G are expected to facilitate charge transfer form surface adsorbed molecules. The results indicate that doping N atoms in PC3-G offers opportunity to tune the properties of the surface. Next, we also conducted the molecular dynamics simulations (MD) to confirm the stability of the binding of P and N atoms on graphene surface by evaluating the thermodynamic stability of PNxCy-G at 300 K. The total simulation time of 2.0 ps is divided into 2500 steps in the NVT ensemble. The system energy and several random structures in the trajectory are presented in supplementary Fig. 3. The calculated results indicate that the single vacancy P doped graphene of PC3-G is shifted downward from the surface. As a result, the structure is deformed. However, no such severe deformation is seen in the substrate of PC3-G. For PN1C2-G and PN2C1-G, the structures are slightly deformed, and no atom is extruded from the substrate, which means that both surfaces remain stable at 300 K without atoms leaving the substrate. Obviously, the PN3-G bond length shows large fluctuations. The P and N bond distances increase during steps 50–90, and P and N bonds form at 100–250 steps. Thus, it is worth noting that the three coordinating N-atoms are not stable. The structures of P binding with neighboring N atoms are stable in PN1C2-G and PN2C1-G for the catalysis.

Adsorption of reaction species on PNxCy-G. The ability of the PNxCy-G graphene sheets to capture O2 and CO molecules around the active site was studied, which is an essential criterion to explore the catalytic activity towards the oxidation of CO. We begin with the understanding of the adsorption performance of the
surface by analysing the adsorption energy and charge information of the gases on the surface which are summarized in supplementary Table 2. The structures of CO and O₂ adsorbed on the surface are shown in Figs. 3 and 4. We now present the calculated results of the P and N co-dopants. We do not investigate the catalytic activity with those on single P-doped graphene (PC₃-G). Our calculations find that the CO molecule binds through physisorption over the PN₁C₂-G, PN₂C₁-G, and PN₃-G sheets, with adsorption energy (E_{ads}) of 0.48, −0.20, and −0.23 eV, respectively. The results indicate that the C–O bond length remains unchanged with respect to the isolated state (1.14 Å) in the adsorbed configurations. Additionally, a small charge transfer from CO to the surface is negligible, which lies in the range of 0.001–0.008 |e|, clearly indicating that physisorption occurs between CO and the surface.

Figure 3. Optimized geometries and corresponding PDOS plots for the adsorption of CO over (a) PN₁C₂-G, (b) PN₂C₁-G, and (c) PN₃-G. All bond distances are in Å. In the PDOS plots, the dashed line indicates the Fermi level (E_F) level, which is set to zero.

Figure 4. Optimized geometries and corresponding PDOS plots for the adsorption of O₂ on (a) PN₁C₂-G (End-on), (b) PN₁C₂-G (Side-on), (c) PN₂C₁-G, and (d) PN₃-G. All bond distances are in Å. In the PDOS plots, the dashed line indicates the Fermi level (E_F) level, which is set to zero.
and the surface. Moreover, the plot of PDOS also confirms weak orbital overlap between the surface and the CO molecule around the Fermi level.

Next, the adsorption of \( O_2 \) molecules on the surface is shown in an optimized geometry. Calculations indicate that the most favored adsorption of \( O_2 \) molecules are chemisorbed over \( PN_1C_2-G \) sheets. Two configurations of \( O_2 \) molecule adsorption over the \( PN_1C_2-G \) sheet exist are found, being the end-on configuration and the side-on configuration of \( O_2 \). The end-on configuration (Fig. 4a) shows formation of an \( O-P \) chemical bond of 1.62 Å and the \( O-O \) bond of approximately 1.38 Å. As illustrated in Fig. 4a (right), the PDOS with the corresponding molecular orbital labels of the end-on configuration reveals that the hybridization of a \( P-p \) orbital and \( O_2-2\pi^* \) orbital slightly overlap above the Fermi level. Figure 4b illustrates the side-on configuration in which \( O_2 \) molecules are nearly parallel to the surface. The \( O-O \) bond distance elongates to 1.56 Å from 1.24 Å in the isolated \( O_2 \) molecule, which suggests an effective weakening of \( O-O \) bond. The \( E_{ads} \) for the end-on configuration is \(-0.54 \) eV, which is less than that of the side-on configuration of \(-1.76 \) eV over \( PN_1C_2-G \). Thus, the side-on configuration exhibits strong adsorption energy due to the \( O-O \) bond is parallel to the graphene surface and forms two chemical bonds with the \( P \) atom. Furthermore, PDOS corresponding molecular orbitals are plotted to show the strong adsorption of \( O_2 \) (Fig. 4b, right). Strong hybridization occurs for the \( P \) atom and the side-on configuration of \( O_2 \) on \( PN_1C_2-G \), which may result in the ready decomposition of \( O_2 \). Charge transfer is approximately 0.685 |e| from the \( P \) atom to the \( 2\pi^* \) states of \( O_2 \), which leads to a broadening and splitting of the \( 2\pi^* \) states, and the elongation of the \( O-O \) bond to 1.56 Å. For \( PN_1C_2-G \), the results show that \( O_2 \) strongly adsorbs with side-on configuration (Fig. 4c) with an adsorption energy of \(-2.83 \) eV. The corresponding \( O-O \) binding distance is 1.58 Å, and there is a significant charge transfer from the surface to the \( O_2 \) molecule, which causes a sizable elongation of the \( O-O \) distance. The PDOS in Fig. 4c (right) displays the strong \( P-p \) orbital and \( O_2-2\pi^* \) orbital hybridization. By contrast, we found that \( O_2 \) molecules over \( PN_1-G \) dissociate with about 2.61 Å elongation of the \( O-O \) distance. The elongation of \( O-O \) results in the \( P-N \) bond-breaking apart by about 2.75 Å. The adsorption energy is remarkably enhanced to \(-4.58 \) eV. As the result of removing a repulsive interaction from the negatively charged \( O \) atoms. The adsorption energy and charge transfer values increase with \( N \) coordination to the \( P \) atom. Additionally, the adsorption of \( O_2 \) molecules over \( PN_3-G \) destroys bond of \( P-N \) because the positive charge on the \( P \) atom is too large, indicating a significant tendency of this site to break incoming \( O_2 \) molecules. Therefore, by increasing the coordination number of \( N \) atoms, the positive charge on the \( P \) increases, this phenomenon that does not benefit the adsorption of electron-rich molecules. Based on results indicate that the proper coordination of two instead of three \( N \) atoms around the \( P \) atom on the surface should benefit \( O_2 \) adsorption. Next, we also investigated the electron density difference of \( PN_2C_1-G \) after the \( O_2 \) molecules are adsorbed (supplementary Fig. 5). The results indicate an electron transfer from the surface to the adsorbed \( O_2 \) molecule. The light blue and yellow in the electron density difference indicate weak orbital overlap between the surface and the \( CO \) molecule, which means a side-on configuration. Thus, as well-known possible reaction mechanisms for the oxidation of \( CO \) to \( CO_2 \) over a \( PN_1C_2-G \) nanosheet are studied via the Langmuir–Hinshelwood (LH), Eley–Rideal (ER), and New Eley–Rideal (NER) reactions29,30.

**Possible mechanisms for CO oxidation.** \( O_2 \) molecule on \( PN_1C_2-G \) exhibits stronger adsorption than \( CO \). Thus, as well-known possible reaction mechanisms for the oxidation of \( CO \) to \( CO_2 \) over a \( PN_3C_1-G \) nanosheet are studied via the Langmuir–Hinshelwood (LH), Eley–Rideal (ER), and New Eley–Rideal (NER) reactions29,30. In the ER mechanism pathway, the \( O_2 \) molecule first adsorbs on the catalytic surface, and the adsorbed \( O_2 \) molecule is attacked by \( CO \) to form a \( CO_2 \) molecule via a \( CO_3 \) intermediate. For the LH mechanism, reaction will start by the co-adsorption of \( O_2 \) and \( CO \) molecules form a peroxo-type \( OOCO \) intermediate, which then dissociates to form a \( CO_2 \) molecule. Otherwise, the NER mechanism involves the co-adsorption of two \( CO \) molecules, first physisorbed over the pre-adsorbed \( O_2 \) molecule. Next, the physisorption of two \( CO \) molecules is close to the pre-adsorbed \( O_2 \) to forms an \( OOCO \) intermediate. Finally, the \( OOCO \) dissociates to form two \( CO_2 \) molecules. These mechanisms are investigated in detail to find the preferred reaction pathway for \( CO \) oxidation.

**The 1st oxidation of \( CO \) via ER mechanisms.** We first investigated the ER mechanism for \( CO \) oxidation. Figure 5a, b present the energy profiles for \( PN_1C_2-G \) and \( PN_2C_1-G \); the initial structure for both surfaces is a side-on configuration. Unfortunately, we found the dissociation of the \( O_2 \) molecule on \( PN_3C_1-G \); therefore, we do not consider the \( CO \) oxidation via an ER mechanism on the \( PN_3C_1-G \). Additionally, the end-on configuration of \( O_2 \) on \( PN_2C_1-G \) as initial is ignored because when \( CO \) approaches the adsorbed \( O_2 \), the \( O_2 \) configuration changes from end-on to side-on, as shown in supplementary Fig. 7. Therefore, the only side-on configuration of \( O_2 \) prefers to occur the \( CO \) oxidation via ER mechanism. For this mechanism to proceed, the \( CO \) is first close to the pre-adsorbed \( O_2 \) on the \( P \) atom on the surface. In the physisorbed initial state (\( IS-ER \)), \( CO \) is 3.01 Å from the \( O_2 \) in \( PN_1C_2-G \) and is 3.30 Å from \( PN_2C_2-G \); the \( O-O \) bond distance remains unchanged. Next, \( CO \) attacks into the \( O-O \) bond and forms the \( CO_2 \) structure as an intermediate (\( Int1-ER \)). The activation energy in this step is needed to form \( CO_2 \) via the transition state (\( TS1-ER \)) for \( PN_1C_2-G \) and \( PN_2C_1-G \), approximately 0.60 eV and 0.29 eV, respectively. Consequently, the \( TS1-ER \) for \( PN_1C_2-G \) is significantly more stable with stronger \( O-C-O \) bonds (2.18 and 2.13 Å) and \( O-P-O \) bonds (1.58 and 1.51 Å), see Fig. 5b. In the next step, the \( CO_2 \) intermediate dissociates to form the \( CO_3 \) molecule via \( TS2-ER \) with an activation energy of 0.29 eV and 0.26 eV for \( PN_1C_2-G \) and \( PN_2C_1-G \), respectively. Finally, the \( CO_2 \) molecule desorbs, and one \( O \) atom still remains adsorbed to the \( P \) atom. Figure 5a, b indicate that the oxidation of \( CO \) via the ER mechanism is highly exothermic over \( PN_1C_2-G \) and \( PN_2C_2-G \). We suggest that in the ER mechanism, \( CO \) oxidation on \( PN_1C_2-G \) is more favorable than \( PN_2C_2-G \), according to the activation energy barriers.
The 1st oxidation of CO via the LH mechanism. Now we shift our attention to CO oxidation via the LH mechanism. The most stable co-adsorption configuration of CO and O₂ molecules in their initial states. We found that only PN₁C₂-G started with the co-adsorption of CO and O₂ molecules on the surface (Supplementary Fig. 11). In its initial state (IS-LH), O₂ is chemisorbed on the P atom and adopts a side-on configuration. CO is tilted over the surface and binding at the P atom with a bond distance of 3.33 Å. Note that the total adsorption energy of CO and O₂ in this configuration is considerable about −3.09 eV. Moreover, the positive charge on phosphorus increases from 0.059 |e| in the side-on configuration of O₂ on PN₁C₂-G to 1.342 |e| in the co-adsorbed configuration. Next, one of the P–O bond breaks, allowing CO to approach the P atom more closely, forming TS₁-LH, providing the four-membered ring (OOCO) intermediate (Int₁-LH) with an activation energy of 0.62 eV. Finally, the O–O and P–C bonds of Int₁-LH lengthen by 1.83 Å and 2.62 Å, respectively. Then, CO₂ molecule releases, leaving one O-atom remains adsorbed on the P atom at the surface via the transition state TS₂-LH with the significant activation energy of 0.86 eV.

The 2nd oxidation of CO via direct CO₂ formation (pathway A). After desorption of the first CO₂, a single O* atom still remains bound to a P atom on the surface. We further investigated the second step of CO oxidation which is direct CO₂ formation. In pathway A (Supplementary Fig. 12), the corresponding initial state (IS-2A), the remaining O* atom interacts with an incoming CO molecule. First, the CO is physisorbed over the pre-adsorbed O* atom with an O*–CO binding distance of 3.03 Å for PN₁C₂-G and 3.12 Å for PN₂C₁-G. Then, CO approaches the O* atom to form CO₂. The P–O bond distance is elongated to 1.86 Å for PN₁C₂-G and 1.85 Å for PN₂C₁-G. The results show that the residual O* is highly chemisorbed over the P atom, with adsorption energies of −4.86 eV (PN₁C₂-G) and −4.53 eV (PN₂C₁-G), resulting in high energy barriers of 0.71 eV (PN₁C₂-G) and 0.98 eV (PN₂C₁-G) to release the CO₂ via transition state TS₁-2A.
The 2nd oxidation of CO via POCC-ring intermediate (pathway B). We investigated the second step of CO oxidation, CO$_2$ formation via the POCC-ring intermediate as shown in pathway B (Fig. 6). For PN$_2$C$_2$-G, CO bonds to the surface at nearest C of P atom through C-bound, bringing two oxygen atoms close together and causing a strong repulsion which requires an energy barrier of 2.97 eV to form a POCC-ring intermediate. Surprisingly, when the N atom is added to the surface (PN$_2$C$_1$-G), CO is more likely to attach the remaining O* atom rather than the surface. As a result, two oxygen atoms are far apart with no repulsion, allowing the formation of the POCC-ring intermediate via TS2-2B, which has a significantly lower energy barrier of 0.25 eV. The second CO$_2$ molecule is then released via TS3-2B, which has an activation energy of 1.11 eV for PN$_1$C$_2$-G and 0.08 eV for PN$_2$C$_1$-G. Furthermore, PDOS with the corresponding molecular orbital is plotted for the IM-2B intermediates in pathway B. The results show that the POCC-ring intermediate displays weak hybridization of the P-p orbital and 2π* orbital for PN$_2$C$_1$-G. This leads to small activation energy to break off the P–O bond on the PN$_2$C$_2$-G surface (Supplementary Fig. 13b). In addition, the reaction energy obtained for PN$_2$C$_1$-G is tiny at 0.08 eV, which clearly indicates the stability of the structure. Thus, a CO$_2$ molecule forms and is quickly released from the surface at room temperature.

The oxidation of CO via the NER mechanism. The energy profile of the NER mechanism involves simultaneous 1st and 2nd oxidation (Supplementary Fig. 14). In its initial state (IS-NER), two CO molecules are first physisorbed over the pre-adsorbed O$_2$ molecule. The O–O bond distance of O$_2$ lengthens until the five-membered ring intermediate (Int1-NER) forms via TS1-NER by overcoming the activation energies of about 0.50 eV and 0.34 eV for PN$_1$C$_2$-G and PN$_2$C$_1$-G, respectively. Next, the C–C bond of the five-membered ring intermediate breaks, leading to the formation of two CO$_2$ molecules via TS2-NER. The dissociation of C–C bonds of Int1-NER is the rate-determining step that requires high activation energy of 1.46 eV for PN$_1$C$_2$-G and 1.19 eV for PN$_2$C$_1$-G.

Rate constants. Our calculations found that CO oxidation reaction is catalyzed by two coordinated N atoms and single vacancy P-embedded graphene via ER mechanism, involving small activation energy (0.26 eV). Importantly, the catalytic model is used to obtain the rate constants of reaction. Thus, calculating the reaction rate of reaction are carried out by microkinetic simulation. The reaction rate for CO oxidation reaction on PN$_1$C$_2$-G
and PN$_{2}$C$_{1}$-G surface as function of temperature are present in Fig. 7. The results show that ER mechanism on PN$_{2}$C$_{1}$-G surface displays much greater activity compared to PN$_{1}$C$_{2}$-G surface. The initial temperature of the reaction on PN$_{2}$C$_{1}$-G surface is about 350–400 K, which will start the reaction. Therefore, the two coordinated N atoms on single vacancy P-embedded graphene of PN$_{2}$C$_{1}$-G are more likely to occur at room temperature via ER mechanism, we found that temperature of the reaction increases with an increase of reaction rate for CO oxidation reaction. Additionally, the production rate of CO$_{2}$ on both surface as function of temperature is present in Fig. 8. The ER mechanism on PN$_{2}$C$_{1}$-G surface exhibits a great production at maximum rate with the optimum temperature of 600 K (Fig. 8b), whereas the optimum temperature of PN$_{1}$C$_{2}$-G surface is dramatically increase to 1750 K (Fig. 8a). These results correspond to the rate determining step of overall reaction on PN$_{1}$C$_{2}$-G and PN$_{2}$C$_{1}$-G surfaces which are calculated to be 0.26 eV and 2.97 eV, respectively indicating that CO oxidation is remarkably favorable on PN$_{2}$C$_{1}$-G and hardly performed on PN$_{1}$C$_{2}$-G surface.

Moreover, we considered the O$_{2}$ adsorption kinetic study. A plot of Gibbs free energy ($G_{ads}$) value and temperature (T) of O$_{2}$ reveal that $G_{ads}$ decreases with an increase of T (Supplementary Fig. 15). The result predicts that the O$_{2}$ molecule can adsorb easily in PN$_{2}$C$_{1}$-G at 370 K, while O$_{2}$ molecule can adsorb on PN$_{1}$C$_{2}$-G and PN$_{3}$-G at 450 K and 530 K, respectively. Thus, this result also supports that CO oxidation can occur in PN$_{2}$C$_{1}$-G at low temperatures.

**Catalytic performance of PN$_{x}$C$_{y}$-G.** PN$_{x}$C$_{y}$-G sheets, where x and y = 1 and 2, exhibit excellent catalytic performance for CO oxidation due to the synergistic effect of P and N atoms on the graphene surface. In the investigation of adsorption of O$_{2}$ and CO on P and N co-doped graphene, the P and N doping models exhibit appropriate activities to adsorb O$_{2}$ and are catalysts for the oxidation of CO. Moreover, we found that the O$_{2}$ molecule shows intense adsorption energy on the PN$_{2}$G surface. Therefore, P and three coordination N atoms are not beneficial for the adsorption of electron-rich molecules because of the additional positive charge on the P
atom. Additionally, the adsorption of O₂ on the PNₓₓCᵧᵧ-G surface breaks the bond between P and N on the surface. Moreover, G_ads value of O₂ molecule associated T indicates that O₂ molecule activates easily in PNₓₓCᵧᵧ-G at 370 K, which is much lower than PN₁₁C₂-G and PN₁₁-G. The above results reflect that the catalytic performance of the first and second steps for CO oxidation on the PNₓₓCᵧᵧ-G surface via the ER mechanism involves activation energy of less than 0.50 eV. Hence, based on these results, we find that the ER mechanism should be more favorable than the LH and NER mechanisms for the oxidation of CO molecules over a PNₓₓCᵧᵧ-G surface. We compared the activation energies of the rate-determining step for CO oxidation on PNₓₓCᵧᵧ-G with those on a different metal-free graphene-based catalyst (Supplementary Table 3). We note that the calculated small activation energy for the ER mechanism on PNₓₓCᵧᵧ-G is comparable with those on P-doped graphene. The results indicate that an increase in the catalytic activity of P and N co-doped graphene for CO oxidation is achievable by two-coordinated N atoms to the P atom on graphene.

Conclusion
The effects of P and N co-doping and N dopant concentration on catalytic activity of graphitic PNₓₓCᵧᵧ-G, where x and y = 0, 1, and 2, toward CO oxidation by O₂ are investigated by DFT calculations. The results show that N-doped single vacancy P-embedded graphene can considerably enhance the surface reactivity of graphene compared to P-doped and N-doped species. The calculated results of the surface properties are related to the large electronegativity difference among the P, N, and C atoms, which induces a positive charge on the P atom. Additionally, two and three coordinated N atoms doping exhibit the small energy gap between valence and conduction band due to the conduction band shifts down to Fermi level. Thus, increasing two or three coordinated N to P can facilitate charge transfer from the surface onto incoming gas molecules and greatly improve graphene's catalytic activity. However, three coordinated N atoms of PNₓₓ-G show a weak interaction, easily deformed and extruded from the substrate. On the other hand, the interaction between the O₂ molecule and PNₓₓ-G is strong as shown in the calculated adsorption energy, suggesting that CO oxidation cannot be initiated over these surfaces. Moreover, Gibbs free energy (G_ads) of O₂ molecule adsorbs on PNₓₓ-G surface at high temperature (530 K), while the temperature for adsorption of O₂ molecule on PNₓₓCᵧᵧ-G and PNₓₓCᵧᵧ-G are 450 K and 370 K, respectively. The synergistic effect of P and two or three coordinated N atoms effectively improves the catalytic activity for excellent catalytic performance in CO oxidation. PNₓₓCᵧᵧ-G catalyzes CO via the ER mechanism at 0 K to overcome the very low energy barrier of 0.26 eV for the first and 0.25 eV for the second CO oxidation process, then releasing 2 molecules of CO₂. The thermodynamic study reveals that CO oxidation can spontaneously take place on PNₓₓCᵧᵧ-G at room temperature. The calculated rate-determining step via ER mechanism of PNₓₓCᵧᵧ-G at 298.15 K is about 0.77 eV. The reaction rate at 298.15 K is calculated to be 5.36 × 10¹⁶ mol s⁻¹. Our findings also indicate that for the CO oxidation reaction over PNₓₓCᵧᵧ-G and PNₓₓCᵧᵧ-G, the ER mechanism is more favorable than the LH and NER mechanism. Moreover, the calculated activation energy for the CO oxidation reaction through the ER mechanism is comparable or even smaller than those of metal-free-based catalysts. Therefore, N co-doped on single vacancy P-embedded graphene show effective catalytic for CO oxidation reaction. Our new finding provides guidelines for designing highly efficient metal-free catalysts.

Data availability
No datasets were generated or analysed during the current study.

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Competing interests
The authors declare no competing interests.

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