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Theoretical study of quantum emitters in two-dimensional silicon carbide monolayers

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I. INTRODUCTION

Two-dimensional (2D) materials have recently received much attraction in the scientific communities because of their unique properties and extensive applications. A prominent aspect of 2D materials is their applications in quantum technologies where single photons are essential. Observation and investigation of single photons in 2D materials such as transition metal dichalcogenides, WO3, and GaSe [1–7], has raised a great interest toward this class of materials in the field of single-photon emitters (SPEs). SPEs in 2D materials are applicable in many quantum technologies ranging from quantum nanophotonics to quantum sensing and quantum information processing [8]. In such materials, the 2D nature of the host considerably improves the photon-extraction efficiency, provides more control over the defect implantation techniques, eases coupling to the waveguides, and provides compatibility with other 2D materials [9]. These advantages have inspired researchers to search and find 2D materials in which all the desired properties of an efficient single-photon source are met. Over the past few years, group IV semiconductors have shown significant potential to host SPEs, in such a way that most ideal single-photon sources were investigated just in diamond and silicon carbide (SiC) [10,11]. Among these traditional three-dimensional (3D) bulk materials, SiC not only emits room temperature single photons but also provides the brightest nonclassical light ever [12,13]. The advantages of 3D SiC in hosting SPEs makes one consider the investigation of the local point defects in its 2D form as potential color centers.

Even though the fabrication of 2D-SiC is still challenging [14–18], the recent observation of SiC nanograins in graphene oxide pores [18] and investigation of quasi-two-dimensional SiC [17] affirm that the fabrication of two-dimensional SiC is about to emerge. Besides, theoretical calculations reveal that many possible 2D structures of SiC are probable in which Si0.5C0.5 structure is the most stable one [19]. Despite the preference of sp3 hybridization of the Si atoms, the Si0.5C0.5 structure, which here on we call 2D-SiC, is predicted to be flat with sp2 hybrid bonds. The band gap of this structure is larger than 3 eV making it an appropriate host for color centers. Considering the high potential of bulk SiC in producing color centers, the predicted wide band gap of 2D-SiC and the superiority of 2D materials in some applications, defects in two-dimensional SiC are expected to be capable of emitting ideal single photons.

In this work we present a study on electronic and optical properties of some favorable defects in 2D-SiC utilizing first-principles calculations assisted by group theoretical analysis to explore SPEs. The study includes vacancy, antisite, substitutional, and Stone-Wales (SW) defects. To investigate potential quantum emission defects, we first calculate zero-phonon-line (ZPL) energy for all possible transitions. Afterwards, we evaluate the Huang-Rhys (HR) factor and the related photoluminescence spectrum for the available transitions in different charge states. The calculated HR values and the related Debye-Waller factors guarantee that the Stone-Wales defects have a high potential of performing as a promising single-photon emitter.
Implementing this method in different simulation packages DFT energy functional. This constraint enforces the desired done by adding a Lagrange multiplier term to the traditional calculation of the band gap and the charge transition levels of intermediate reliable results. The HSE06 hybrid functional calculates the band gap and the charge transition levels of group-IV semiconductors within 0.1 eV accuracy [24].

The motivation behind HSE06 hybrid functionals is the observation that Hartree-Fock overestimates band gaps and semilocal density functionals underestimate them. Therefore, the hybrid exchange functional of Heyd, Scuseria, and Ernzerhof (HSE06) is applied to overcome this problem [22,23].

Within the CDFT method, the ions are relaxed to reach the ground state electronic structure is obtained by performing geometry relaxation in which internal positions of atoms are relaxed until forces on them are smaller than 0.02 eV/Å. Within the CDFT method, the ions are relaxed to reach the global minimum of adiabatic potential energy surface in the excited state.

The PL spectrum is calculated within the HR theory which was proposed by Huang and Rhys in 1950 [29]. One important quantity in HR theory is the partial Huang-Rhys factor. This factor helps us in assessing a point defect as a good single-photon emitter. The factor is given by

$$ S_k = \frac{\omega_k q_k^2}{2\hbar}, $$

where $\omega_k$ is frequency of the $k$th phonon mode, $\hbar$ is the reduced Planck constant, and $q_k$ is defined as

$$ q_k = \sum_{\alpha,i} m_\alpha^{1/2} (R_{\alpha,i}^{(e)} - R_{\alpha,i}^{(g)}) \Delta R_{k,\alpha,i}, $$

where $m_\alpha$ is the mass of atom $\alpha$, $R_{\alpha,i}^{(e)}$ and $R_{\alpha,i}^{(g)}$ are equilibrium atomic coordinate of atom $\alpha$ along the direction $i$ in the excited state and the ground state, and $\Delta R_{k,\alpha,i}$ is the normalized displacement vector of atom $\alpha$ along the direction $i$ in phonon mode $k$. Sum of the partial HR factor over all phonon modes $k$ gives the total HR factor. This quantity determines coupling between electronic and vibrational states and characterizes the phonon side band. The PL intensity is defined as

$$ I(\hbar w) = C w^3 A(\hbar w), $$

where $C$ is the normalization constant and $A(\hbar w)$ is the optical spectral function given by

$$ A(\hbar w) = \frac{1}{2\pi} \int_{-\infty}^{\infty} G(t) e^{i\omega t - \gamma |t|} dt. $$

Here $\gamma$ is linewidth of the ZPL. $G(t)$ is the generating function and is defined as

$$ G(t) = e^{S(t) - S_{\text{tot}}}, $$

where $S(t)$ is the Fourier transform of the partial HR factor, defined as

$$ S(\hbar w) = \sum_k S_k \delta(\hbar w - \hbar w_k), $$

and $S_{\text{tot}}$ is the total HR factor. The Debye-Waller (DW) factor describes the ratio of the emission of coherent photons vs total number of emitted photons including the phonon assisted ones which compromise the coherence. This factor is related to the HR factor and determines the weight of the ZPL.

Here the PL spectrum and the HR factor are calculated based on Refs. [30,31]. Since the PBE functional provides the PL spectrum in good agreement with the HSE06 hybrid functional, by applying this functional the geometry is relaxed.
until all forces are smaller than $10^{-3}$ eV/Å, then density functional perturbation theory (DFPT) within the VASP code is used to obtain the phonon eigenfrequencies and eigenvectors. Calculation of the HR factor is very expensive due to its requirement to the full phonon spectrum. Therefore its calculations is not computationally affordable for all of the surveyed defects. For this reason, we single out a few most promising color center candidates in our search among the point defects by using their $\Delta Q$ parameter as a filtering parameter. The calculation of $\Delta Q$ is not computationally expensive, nonetheless, its behavior is proportional to that of the HR factor. In fact, $\Delta Q$ specifies the atomic structure change during the excitation. To calculate it, we apply one-dimensional configuration coordinate formulation which is represented by

$$\Delta Q^2 = \sum_{\alpha,i} m_{\alpha} \Delta R_{\alpha,i}^2,$$

where $\Delta R_{\alpha,i}$ is $R_{\alpha,i}^{(e)} - R_{\alpha,i}^{(g)}$. As mentioned above, the high (low) values of $\Delta Q$ correspond to high (low) values of the HR factor. The stability of charged defects is determined by (low) values of $\Delta Q$. Calculation of the HR factor is very expensive due to its requirement to the full phonon spectrum. Therefore its calculations is not computationally affordable for all of the defects.

### Table I. The calculated ZPL energy and $\Delta Q$ value for defects possible transitions using a HSE06 hybrid functional in a 6 x 6 supercell. The superscripts "up" and "down" refer to spin up and spin down channels.

| Defect        | $E_{\text{ZPL}}^{\text{up}}$ (eV) | $E_{\text{ZPL}}^{\text{down}}$ (eV) | $\Delta Q$ (Å amu$^{-1/2}$) |
|---------------|----------------------------------|-----------------------------------|----------------------------|
| $V_C^+$       | 2.59                             | -                                 | 2.41                       |
| $V_C^-$       | -                                | 0.59                              | 1.23                       |
| $V_{Si-V_C}$  | 0.917                            | -                                 | 1.25                       |
| $V_{Si-V_C}^+$| 1.76                             | -                                 | 2.16                       |
| $V_{Si-V_C}^-$| 1.02                             | -                                 | 1.56                       |
| $V_{Si-V_C}^+$| 2.21                             | -                                 | 1.20                       |
| $V_{Si-V_C}^-$| -                                | 1.51                              | 1.08                       |
| $V_{C-C_Si}^+$| 1.48                             | -                                 | 0.83                       |
| $V_{C-C_Si}^-$| 1.05                             | -                                 | 0.85                       |
| $V_{C-C_Si}^+$| 0.86                             | -                                 | 1.25                       |
| $V_{C-C_Si}^-$| 1.69                             | -                                 | 0.88                       |
| $V_{C-C_Si}^+$| 2.32                             | -                                 | 0.93                       |
| $V_{C-C_Si}^-$| -                                | 2.18                              | 0.63                       |
| $V_Si$        | -                                | 0.41                              | 0.87                       |
| $V_{Si}^+$    | -                                | 1.99                              | 1.03                       |
| $V_{Si}^-$    | -                                | 1.05                              | 0.94                       |
| $V_{Si}^+$    | -                                | 0.88                              | 0.58                       |
| $V_{Si}^-$    | -                                | 1.90                              | 1.05                       |
| $V_{Si}^+$    | -                                | 1.97                              | 1.11                       |
| $V_{Si}^-$    | -                                | 2.03                              | 1.42                       |
| SW            | 1.47                             | -                                 | 0.46                       |
| SW$^+$        | 1.63                             | -                                 | 0.49                       |
| SW$^-$        | -                                | 1.60                              | 0.53                       |
| SW-SiC        | 1.54                             | -                                 | 0.39                       |
| SW-SiC$^+$    | 1.77                             | -                                 | 0.40                       |
| SW-SiC$^-$    | 2.64                             | -                                 | 0.46                       |
| SW-SiC$^+$    | -                                | 3.35                              | 0.35                       |
| SW-SiC$^-$    | -                                | 3.29                              | 0.22                       |
| SW-SiC$^+$    | -                                | 1.50                              | 0.42                       |
| SW-SiC$^-$    | -                                | 1.65                              | 0.53                       |
| SW-C_Si       | 1.32                             | -                                 | 2.32                       |
| SW-C_Si$^+$   | 2.28                             | -                                 | 0.63                       |
| SW-C_Si$^-$   | 1.73                             | -                                 | 0.57                       |
| SW-C_Si$^+$   | 1.33                             | -                                 | 2.51                       |
| SW-C_Si$^-$   | 2.51                             | -                                 | 0.81                       |
| SW-C_Si$^+$   | -                                | 1.67                              | 0.48                       |
occupations, and then the spin state of the collective electrons, and finally the tensor product of the spatial wave function with the spin part. Here the neutral charge defects can only assume singlet spinor in their ground state and both singlet and triplet states in the electronic excited state. All other combinations are rejected by Pauli’s exclusion principle. Meanwhile, the positively charged defects are only spin doublet.

The group theory allows us to predict potentially nonzero matrix elements of the Hamiltonians that are perturbatively included in the analysis. The spin-orbit interaction is one of the crucial interactions that yet remains a perturbation in the system as SiC is composed of relatively light atom species. The interaction induces nonradiative transitions between the multielectron states. Another critical effect which lies at the heart of our analysis is the electric dipole interaction that determines dark and bright states. Those states that their dipole moment can couple to the ground state via the external electric field, provided by electromagnetic radiation, determine the selection rules [35,36]. In this part of study, the value of matrix elements $\langle \psi | O | \phi \rangle$ is vanishing if their total irreducible representation is not of totally symmetric irreducible representation, here $A_1$ and $A'$ for the $C_{2z}$ and $C_r$, respectively. In the mathematical expression $\Gamma(\psi) \otimes \Gamma(O) \otimes \Gamma(\phi) \not\supset \Gamma_1$, where $\Gamma(X)$ is the irreducible representation of the object $X$ and $\Gamma_1$ is the totally symmetric irrep. The selection rules are obtained by studying the electric dipole interaction $H_{dp} = -\mathbf{d} \cdot \mathbf{E}$, where $\mathbf{d} = -\varepsilon(x, y, z)$ is the dipole moment of the electronic state and $\mathbf{E}$ is the electric field vector. $\mathbf{d}$ transforms like a polar vector, and its components have a different irrep as listed in the character tables. The polarization of radiative transitions is thus predicted by inspecting those components with nonvanishing matrix elements.

III. RESULTS AND DISCUSSIONS

In our DFT calculation we find that 2D-SiC remains in a plane which agrees with previous works [18,19]. The Si-C bond distance is calculated to be 1.78 Å with PBE functional and 1.77 Å with HSE06 hybrid functional. We evaluate a large band gap of 3.58 eV for 2D-SiC with HSE06 and 1.77 Å with HSE06 hybrid functional. We evaluate a bond distance is calculated to be 1.78 Å with PBE functional respectively.

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per atom). Then the carbon chemical potential can be obtained from $\mu_{\text{SiC}} = \mu_{\text{Si}} + \mu_{\text{C}}$ where $\mu_{\text{SiC}}$ is the total energy of SiC primitive cell. In C-rich condition, the carbon chemical potential is derived from graphite (total energy per atom), and for the silicon chemical potential we use the equilibrium condition as explained. The results for HSE06 hybrid functional are presented in Fig. 3. The obtained formation energy shows that the negative charge state is not stable for any of the Stone-Wales defects as the $(0/−)$ charge transition levels for SW, SW-SiC, and SW-CSi defects are at $\text{EV} + 4.00$, $\text{EV} + 4.30$, and $\text{EV} + 4.19$ eV, respectively, where $\text{EV}$ is the valence band maximum. Unlike the negative charge states, the neutral charge states are stable as the $(+/0)$ charge transition levels are at $\text{EV} + 0.43$, $\text{EV} + 0.59$, and $\text{EV} + 0.23$ eV, respectively. We also consider the positive charge state of these defects stable because their highest occupied molecular orbital (HOMO) lies between the $(+/0)$ charge transition level and the valence band maximum within the band gap.

One expects when the heat of formation of SiC-2D lattice is negative, the formation energy of SW-SiC (SW-CSi) defect in Si-rich (C-rich) condition to be lower in energy than in the C-rich (Si-rich) condition. But the trends obtained in Fig. 3 are opposite, and it is because the heat of formation of 2D-SiC is positive (0.56 eV) and this material is only a metastable form of silicon carbide. The heat of formation is obtained from $\Delta H_f = \mu_{\text{2D-SiC}} - (\mu_{\text{bulk Si}} + \mu_{\text{graphite C}})$ where $\mu_{\text{2D-SiC}}$ is the total energy of 2D-SiC primitive cell, $\mu_{\text{bulk Si}}$ is the total energy per atom of bulk silicon, and $\mu_{\text{graphite C}}$ is the total energy per atom of graphite [37]. Another point is that SW-CSi defect could be about 2 eV lower in formation energy than the SW-SiC defect in stoichiometric conditions, simply because the C atom likes the $sp^2$ configuration much more than the Si atom does. Thus, changing the C/Si ratio (Si-rich vs C-rich condition) does not alter this order but only closes the energy spacing.

Before going through the detailed $ab initio$ calculation on these defects, we provide a group of theoretical calculations with an emphasize on the electronic structure and the possible transitions, both radiative and nonradiative. The substitutional SW defects have a $C_{2v}$ symmetry and irr of their orbitals are as assigned in Fig. 4. The neutral charge defects have a fully occupied singlet orbital in their ground state. Thus, we expect a spin-singlet state for these cases. In the excited states, however, both singlet and triplet spin states are allowed that divides the radiative transition channels into triplet and singlet as the dipole transitions are spin state preserving in the zeroth order of spin-orbit Slater states. This allows us to construct the electronic structure of the few lowest states and determine the polarization of the radiative transitions according to the matrix element symmetries (see Fig. 2 for the structure as well as the transitions). The positively charged defects provide only one electron in the band gap, which implies the one have to expect spin-doublet states. We find that the order of orbitals is slightly shuffled by subtraction of one electron from the defect. The electronic structure, thus, behaves differently. Our analysis on the spin-orbit interaction suggests that nonradiative transition through the shelving states is also possible. The
FIG. 4. Kohn-Sham ground state electronic levels of (a) SW, (c) SW-SiC, and (e) SW-C_{Si} defects. Occupied and unoccupied levels are shown with solid black lines and blue dashed lines. Charge density plots for neutral defect states are displayed in (b) SW, (d) SW-SiC, and (f) SW-C_{Si}. The symmetry of molecular orbitals are shown both next to the energy levels and the charge density plots. The \( C_{2v} \) symmetry labels are also used for the SW defect.

pure SW defect has a reduced symmetry of \( C_{v} \), which results in an increased dipole transition probability. For this reason we expect brighter emissions. However, note that for the sake of clarity we have assigned \( C_{2v} \) irr labels to the MOs and the multielectron states in Fig. 2 as well as Fig. 4.

We recalculate the electronic structure of these defects in neutral and positive charge states in an \( 8 \times 8 \) supercell. Their electronic structure is shown in Fig. 4. If we take a look at this structure, we will find that all the neutral charge states and all the positive charge states are similar. It is because carbon and silicon belong to the same group in the periodic table of the elements as it was demonstrated in group-IV vacancy color centers in diamond [25]. Localization of charge density plot is also displayed in Fig. 4. It determines electronic defect states in the band gap. In this massive supercell we inspected the defects viability in emitting single photons by evaluating the ZPL energy and the HR factor for every electronic transition. These values were displayed in Table II. The values of DW factor are up to 50% in the 2D-SiC monolayer. It confirms the high quantity of these defects in producing single photons. We should mention that these values would be considerably higher in a multilayer of 2D-SiC because the van der Waals forces between layers decrease the structural changes during the excitation, which leads to higher amounts of DW factor. This difference was also observed in hexagonal boron nitride [38]. In Table II the ZPL energies range from 1.4 to 3.3 eV. It demonstrates that observation of single photons would be possible in visible and near-infrared regions which makes them promising candidates with quantum functionalities in quantum communication, quantum information processing, and biological sensing. For every defect we also plotted the PL spectrum of the transition with the lowest value of the HR factor, which is shown by red color in Fig. 5. The PL spectrum can provide a support for the future experimental investigation of single-photon sources which is related to Stone-Wales defects in 2D-SiC.

Finally, it is worth mentioning that usually the 2D structures of materials are grown on or transformed onto proper substrates [39–41]. Hence, including the effect of substrate surface on the SPEs demands further investigations, which remains an open subject for future studies. We note here that recent calculations on color centers in hexagonal boron nitride have demonstrated that the number of boron nitride layers has minimal effect on the ZPL of the color centers [36]. Similarly, we expect that 2D-SiC monolayers form weak bonds with the substrate, and thus only cause slight modification in the properties of the localized defect states. Experimental techniques alongside proper choice of substrate could be envisaged for diminishing such surface interactions. For instance, oxidation of bilayer silicene on Ag(111) surface leads to a top layer of silicene which has negligible interaction with the substrate [42]. Also, the intrinsic properties of silicene are accessible by epitaxially growing silicene on metal substrates and then transferring it to an insulating substrate [43]. Therefore, in the case of 2D-SiC, as a hypothetical material with properties similar to silicene, once fabricated upon a proper
substrate with a small interaction our results apply with slight modifications. In fact, if the 2D-SiC layer does not form any covalent bond to the substrate or it floats on another 2D-SiC layer, then the effect on the ZPL position would be minimal because the defect states are really localized in the sheet of 2D-SiC.

IV. CONCLUSION AND OUTLOOK

Our first-principles calculation has led us to introduce the most probable single-photon emitter candidates in two-dimensional SiC monolayer. We calculated the ZPL energy, the Huang-Rhys factor, and the photoluminescence spectrum for some selected defects. The values of the HR factor are in the range of 0.74 to 3.32 (Debye-Waller factor of 48% to 4%). Our 

initio analysis demonstrated that Stone-Wales defects (SW, SW-SiC, SW-CSi) in neutral and positive charge states are capable of emitting single photons. The group theory analysis for the SW neutral and charged defects predicted the polarization of radiative and nonradiative transitions, respectively. Increasing dipole transition probability in pure SW defect with lower symmetry convinced us of having brighter emissions in these defects. Our analysis on the spin-orbit interaction suggests that nonradiative transition through the shelving states is also possible. The plotted PL spectra of the transitions with the highest value of the HR factor suggest the following opportunities for future experimental investigation of single-photon sources which are related to the Stone-Wales defects in 2D-SiC.

In this article a novel two-dimensional material is proposed as a host for single-photon sources and actively encourages other scientific groups who are interested in SPEs field to endeavor for the fabrication of 2D-SiC and explore other fascinating properties of this material. We find that typical defects in 2D materials, Stone-Wales defects, are promising quantum emitters in 2D-SiC which may direct researchers to seek other bright emitters in this material. We note that the presence of metastable triplet states may be harnessed as quantum bits in the neutral Stone-Wales defects but further investigations are required to study this phenomenon in Stone-Wales defects and other potential quantum bits in 2D-SiC.

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