Current experimental bounds on stop mass in natural SUSY

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Abstract

Motivated by the recent progress of direct search for the productions of stop pair and sbottom pair at the LHC, we examine the constraints of the search results on the stop ($\tilde{t}_1$) mass in natural SUSY. We first scan the parameter space of natural SUSY in the framework of MSSM, considering the constraints from the Higgs mass, B-physics and electroweak precision measurements. Then in the allowed parameter space we perform a Monte Carlo simulation for stop pair production followed by $\tilde{t}_1 \rightarrow t \tilde{\chi}_1^0$ or $\tilde{t}_1 \rightarrow b \tilde{\chi}_1^+$ and sbottom pair production followed by $\tilde{b}_1 \rightarrow b \tilde{\chi}_1^0$ or $\tilde{b}_1 \rightarrow t \tilde{\chi}_1^-$. Using the combined results of ATLAS with 20.1 fb\textsuperscript{-1} from the search of $\ell + \text{jets} + \not{E}_T$, hadronic $t\bar{t} + \not{E}_T$ and $2b + \not{E}_T$, we find that a stop lighter than 600 GeV can be excluded at 95% CL in this scenario.

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I. INTRODUCTION

Observation of a SM-like Higgs boson around 125 GeV by the ATLAS and CMS Collaborations [1] has had a great impact on the minimal supersymmetric standard model (MSSM), in which the naturalness problem is a key issue [2–8]. For the electroweak naturalness the stops play an important role by cancelling the top quark loop, and thus the LHC search for the stop pair production will shed light on this question in the MSSM. The ATLAS and CMS collaborations have also made searches for supersymmetric particles with about 20 fb$^{-1}$ of data [9–11]. The negative results of sparticle search may indicate the natural SUSY scenario [4–8], in which the first two generations of squarks are heavy and the third generation of squarks are light.

In the framework of MSSM, the fine-tuning can be estimated by the Barbieri-Giudice measure [3]

$$\Delta = \max\{\Delta_p\},$$

$$\Delta_p = \left| \frac{\partial \log M^2_Z}{\partial \log p_i} \right|.$$ (1)

where $p_i$ denotes the soft SUSY-breaking terms that enter the minimization conditions of the Higgs potential [12].

$$\frac{M^2_Z}{2} = \frac{(m^2_{H_d} + \Sigma_d) - (m^2_{H_u} + \Sigma_u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2,$$ (2)

with $\tan \beta \equiv v_u/v_d$, $m^2_{H_d}$ and $m^2_{H_u}$ representing the weak scale soft SUSY breaking masses of the Higgs fields, $\mu$ being the higgsino mass parameter, $\Sigma_u$ and $\Sigma_d$ being the radiative corrections to the tree-level Higgs potential. In order to maintain naturalness, the parameters $\mu$, $m_{H_u}$ and $\Sigma_u$ are expected to be at weak scale, which will impose a constraint on the spectrum of MSSM [6].

$$\mu \lesssim 200 \text{ GeV} \left( \frac{m_h}{125 \text{ GeV}} \right) \sqrt{\frac{\Delta}{5}},$$ (3)

$$\sqrt{m_{\tilde{t}_1}^2 + m_{\tilde{t}_2}^2 + A_t^2} \lesssim 600 \text{ GeV} \sin \beta \ L_\Lambda \left( \frac{m_h}{125 \text{ GeV}} \right) \sqrt{\frac{\Delta}{5}},$$ (4)

$$M_3 \lesssim 900 \text{ GeV} \sin \beta \ L_\Lambda^2 \left( \frac{m_h}{125 \text{ GeV}} \right) \sqrt{\frac{\Delta}{5}},$$ (5)

with $L_\Lambda = \sqrt{3/\log (\Lambda/\text{TeV})}$ coming from the leading-log approximation of the RGE [6]. Of course, in a given model like the MSSM, CMSSM or natural SUSY, the fine-tuning extent...
depends on the parameters appearing in the left sides of Eqs. (3–5), which can be checked by examining the parameter space allowed by current experiments [13–22].

In this work we focus on natural SUSY and examine the constraints of the LHC search results of stop and sbottom [10, 11]. Note that some studies in this aspect have been performed in the literature [23, 24]. However, the study in [23] assumed a special scenario with $A_t = 0$ and $\tan \beta = 10$ and, as a result, the stop decay is much simplified, while the analysis in [24] did not consider the ATLAS sbottom search results. In our study we will consider a more general natural SUSY with more experimental constraints. We will first scan the parameter space of natural SUSY in the framework of MSSM, considering the constraints from the LHC Higgs mass, B-physics and electroweak precision measurements, and then in the allowed parameter space we will perform a detailed Monte Carlo simulation for stop pair production with $\tilde{t}_1 \rightarrow t \tilde{\chi}_1^0$ or $\tilde{t}_1 \rightarrow b \tilde{\chi}_1^+$ and sbottom pair production with $\tilde{b}_1 \rightarrow b \tilde{\chi}_1^0$ or $\tilde{b}_1 \rightarrow t \tilde{\chi}_1^-$ at the LHC, applying the same cuts as in the ATLAS searches. Finally, using the combined results of ATLAS with 20.1 fb$^{-1}$ from the search of $\ell +\text{jets} + \not{E}_T$, hadronic $tt + \not{E}_T$ and $2b + \not{E}_T$, we will figure out the allowed range for the stop in natural SUSY.

We organize the paper as follows. In Sec. II, we scan the parameter space and present the spectrum of natural SUSY allowed by the Higgs mass, B-physics and electroweak precision measurements. In Sec. III we simulate the direct stop/sbottom pair productions and examine their constraints on the parameter space of natural SUSY. Finally, we draw our conclusion in Sec. IV.

II. A SCAN OF THE PARAMETER SPACE

In accordance with the definition of natural SUSY, $\mu$ should have a value at weak scale and the third generation of squarks should not be too far above TeV scale. So we scan these parameters in the following ranges

$$100 \text{ GeV} \leq \mu \leq 200 \text{ GeV}, \quad 100 \text{ GeV} \leq (m_{\tilde{t}_L} = m_{\tilde{b}_L}, \ m_{\tilde{t}_R}) \leq 2 \text{ TeV}. \quad (6)$$

In natural SUSY the gluino mass is supposed to be below several TeV. Since in our study we focus on stop/sbottom direct searches, the gluino mass is not a sensitive parameter, which is fixed at 2 TeV in our scan. The sleptons and first two generations of squarks in natural SUSY are supposed to be heavy, which are all fixed at 5 TeV. For the electroweak gaugino
masses, we use the grand unification relation $M_1 : M_2 = 1 : 2$ and take $M_1 = 1$ TeV (in natural SUSY $M_1$ is usually supposed to be larger than $\mu$ and the lightest neutralino is higgsino-like). Further, we assume $A_t = A_b$ and $m_{\tilde{b}_R} = m_{\tilde{t}_R}$, which in our scan vary in the ranges

$$|A_t| \leq 3 \text{ TeV}, \quad 1 \leq \tan \beta \leq 60, \quad 90 \text{ GeV} \leq M_A \leq 1 \text{ TeV},$$

(7)

where the lower bound of $M_A$ is indicated from LEP and B-decay constraints. Since the component of the stop ($\tilde{t}_1$) will affect its decay modes, we scan the parameter space in two scenarios: (I) $m_{\tilde{t}_R}$ is lighter than $m_{\tilde{t}_L}$; (II) $m_{\tilde{t}_L}$ is lighter than $m_{\tilde{t}_R}$.

In our scan we consider the following constraints:

(1) We require the SM-like Higgs mass in the range of 123–127 GeV. We calculate the Higgs mass with *FeynHiggs2.8.9* [25] and impose the experimental constraints from LEP, Tevatron and LHC with *HiggsBounds-3.8.0* [26].

(2) We require natural SUSY to satisfy various B-physics bounds at 2$\sigma$ level. We use the package of *SuperIso v3.3* [27] to implement the constraints, including $B \rightarrow X_s \gamma$ and the latest measurements of $B_s \rightarrow \mu^+\mu^-$, $B_d \rightarrow X_s \mu^+\mu^-$ and $B^+ \rightarrow \tau^+\nu$.

(3) We require the SUSY prediction of the precision electroweak observable such as $\rho_t$, $\sin^2 \theta_{\text{eff}}^l$, $m_W$ and $R_b$ [28] to be within the 2$\sigma$ ranges of the experimental values.

(4) We require the thermal relic density of the lightest neutralino (as the dark matter candidate) is below the 2$\sigma$ upper limit of the Planck value [29]. We use the code *MicrOmega v2.4* [30] to calculate the relic density.

In Fig. 1 we show the sparticle spectrum in the parameter space allowed by constraints (1-4) in natural SUSY. From the figure we can find the following features and implications. Firstly, for both $m_{\tilde{t}_L} < m_{\tilde{t}_R}$ and $m_{\tilde{t}_L} > m_{\tilde{t}_R}$, the stop ($\tilde{t}_1$) mass is heavier than about 200 GeV. The lower limit of the stop in case of $m_{\tilde{t}_L} > m_{\tilde{t}_R}$ is larger than in the case of $m_{\tilde{t}_L} < m_{\tilde{t}_R}$. The reason is that for $m_{\tilde{t}_L} > m_{\tilde{t}_R}$ the Higgs mass will receive a negative correction proportional to $\cos 2\beta \log(m_{\tilde{t}_L}/m_{\tilde{t}_R})$ [31] and, in order to enhance the Higgs mass to 125 GeV, the splitting between $m_{\tilde{t}_L}$ and $m_{\tilde{t}_R}$ is preferred to be small and a heavier stop mass is favored to balance the negative correction. Secondly, the masses of $\tilde{\chi}_1^+, \tilde{\chi}_1^0$ and $\tilde{\chi}_2^0$ are below 200 GeV and are nearly degenerate, which, due to the soft decay products, will
FIG. 1: Sparticle mass spectrum in the parameter space allowed by constraints (1–4) in natural SUSY.

weaken the constraints from direct electroweak gauginos searches at the LHC. However, this spectrum may strengthen some limits from direct stop/sbottom searches at the LHC since the final states $b\tilde{\chi}_{1}^{+}$ ($t\tilde{\chi}_{1}^{0}$) have the same signatures as $b\tilde{\chi}_{1,2}^{0}$ ($t\tilde{\chi}_{1,2}^{0}$).

III. CONSTRAINTS FROM THE LHC SEARCH OF STOP/SBOTTOM

Since the decay modes of stop and sbottom will affect the implication of direct searches, we first discuss their decay branching ratios. The relevant interactions between stop and neutralinos or charginos are given by [32]

$$\mathcal{L}_{tt\tilde{\chi}_i^0} = \bar{t}_1 t(f^N_L P_L + f^N_R P_R)\tilde{\chi}_i^0 + h.c., \tag{8}$$

$$\mathcal{L}_{tb\tilde{\chi}_i^\pm} = \bar{t}_1 b(f^C_L P_L + f^C_R P_R)\tilde{\chi}_i^\pm + h.c., \tag{9}$$

where $P_{L/R} = (1 \mp \gamma_5)/2$ and

$$f^N_L = -\left[\frac{1}{\sqrt{2}}g_2 [N_{\chi_i^0}]_{i\tilde{W}} + \frac{1}{3\sqrt{2}}g_1 [N_{\chi_i^0}]_{i\tilde{B}}\right] \cos \theta_t - y_t [N_{\chi_i^0}]_{i\tilde{H}_2} \sin \theta_t, \tag{10}$$

$$f^N_R = \frac{2\sqrt{2}}{3}g_1 [N_{\chi_i^0}]_{i\tilde{B}} \sin \theta_t - y_t [N_{\chi_i^0}]_{i\tilde{H}_2} \cos \theta_t, \tag{11}$$

$$f^C_L = y_b [U_{\chi_i^+}]_{i\tilde{H}_1} \cos \theta_t, \tag{12}$$

$$f^C_R = -g_2 [V_{\chi_i^+}]_{i\tilde{W}} \cos \theta_t + y_t [V_{\chi_i^+}]_{i\tilde{H}_2} \sin \theta_t. \tag{13}$$
with \( y_t = \sqrt{2} m_t / (v \sin \beta) \) and \( y_b = \sqrt{2} m_b / (v \cos \beta) \) being the Yukawa couplings of top and bottom quarks, and \( \theta_t \) being the mixing angle between left- and right-handed stops \((-\pi/2 \leq \theta_t \leq \pi/2\)). The neutralino and chargino mixing matrices \( N_{ij}, U_{ij} \) and \( V_{ij} \) are defined in [32]. The interactions of the sbottom with neutralino or chargino can be obtained from above expressions by replacing \( \theta_t \) with \( \theta_b \) and interchanging \( y_t \) and \( y_b \).

![FIG. 2: The scatter plots of the parameter space allowed by constraints (1-4) in natural SUSY, showing the decay branching ratios of stop and sbottom.](image)

In Fig. 2 we display the numerical results of the decay branching ratios of stop and sbottom. From the upper panel we can see that a light stop \((\tilde{t}_1 < 370 \text{ GeV})\) will be dominated by decaying to \( b \chi^+_1 \). When the stop becomes heavier, the \( \tilde{t}_1 \rightarrow t \chi^0_{1,2} \) channels are open and the decay \( \tilde{t}_1 \rightarrow b \chi^+_1 \) is suppressed. For \( m_{\tilde{t}_L} < m_{\tilde{t}_R} \), \( \text{Br}(\tilde{t}_1 \rightarrow b \chi^+_1) \) is less than 50%, and \( \text{Br}(\tilde{t}_1 \rightarrow t \chi^0_1) \) and \( \text{Br}(\tilde{t}_1 \rightarrow t \chi^0_{1,2}) \) are approximately equal which vary between 25% and 50%. While for \( m_{\tilde{t}_L} > m_{\tilde{t}_R} \), \( \text{Br}(\tilde{t}_1 \rightarrow b \chi^+_1) \) is around 50% and \( \text{Br}(\tilde{t}_1 \rightarrow t \chi^0_{1,2}) \) can only
reach 25%. These features can be understood from Eqs. (10–13) in the chiral limit. From those expressions we can see that $\tilde{t}_1$ becomes purely left-handed for $\theta_{\tilde{t}} = 0$ and right-handed for $\theta_{\tilde{t}} = \pm \pi/2$. Since $\tilde{\chi}^0_{1,2}$ are higgsino-like, the couplings $C_{\tilde{t}\tilde{t}\chi^0_{1,2}}$ are proportional to $y_t$ and nearly equal for both $m_{\tilde{t}_L} < m_{\tilde{t}_R}$ and $m_{\tilde{t}_L} > m_{\tilde{t}_R}$. However, the coupling $C_{b\tilde{t}_1\tilde{b}}$ is dominated by the bottom Yukawa coupling $y_b$ for $m_{\tilde{t}_L} < m_{\tilde{t}_R}$ and by the top Yukawa coupling $y_t$ for $m_{\tilde{t}_L} > m_{\tilde{t}_R}$. So, we can infer that when $\tilde{t}_1 \rightarrow t\tilde{\chi}^0_{1,2}$ is kinematically allowed, $Br(\tilde{t}_1 \rightarrow b\tilde{\chi}^+_1)$ will be generally below $Br(\tilde{t}_1 \rightarrow t\tilde{\chi}^0_{1,2})$ for $m_{\tilde{t}_L} < m_{\tilde{t}_R}$ and twice as large as $Br(\tilde{t}_1 \rightarrow t\tilde{\chi}^0_{1,2})$ for $m_{\tilde{t}_L} > m_{\tilde{t}_R}$. For the sbottom decays on the lower panel, they can be understood by similar analysis as above.

In the following, we use the ATLAS direct stop/sbottom search data \cite{10,11} to constrain the parameter space of natural SUSY. The signals of the direct searches and the source of each signal in natural SUSY are shown in Table I. In our calculation we simulate the signals by MadGraph5 \cite{33} and carry out the parton shower and fast detector simulation with PYTHIA \cite{34} and Delphes \cite{35}. We use the anti-$k_t$ algorithm \cite{36} to cluster jets and the MLM scheme \cite{37} to match our matrix element with parton shower. For the cross section of $\tilde{t}\tilde{t}^*/\tilde{b}\tilde{b}^*$ we use the NLO results calculated by the package Prospino2.1 \cite{38}. Before presenting the exclusion limits, in Appendix A we validate our simulations by adopting the same cuts flow of ATLAS and comparing our results to the ATLAS results. We can see that our results are consistent with ATLAS in the reasonable error ranges. Then, we perform the simulation for each survived sample in Fig. 2 and use CL$_s$ method to obtain the 95% exclusion limit. For each channel $i$ after cuts flow, we can define CL$_s^i$ as

$$CL_s^i = \frac{\text{Pois}(n_i|b_i + s_i)}{\text{Pois}(n_i|b_i)}.$$  (14)

| Signals of ATLAS stop/sbottom direct searches | Source of each signal in natural SUSY |
|---------------------------------------------|---------------------------------------|
| $\ell + \text{jets} + E_T$                 | $pp \rightarrow \tilde{t}_1\tilde{t}_1 (\tilde{t}_1 \rightarrow t\tilde{\chi}^0_{1,2})$ |
|                                           | $pp \rightarrow \tilde{b}_1\tilde{b}_1 (\tilde{b}_1 \rightarrow t\tilde{\chi}^-_1)$ |
| $t\bar{t}$(hadronic)$+E_T$                | $pp \rightarrow \tilde{t}_1\tilde{t}_1 (\tilde{t}_1 \rightarrow t\tilde{\chi}^0_{1,2})$ |
|                                           | $pp \rightarrow \tilde{b}_1\tilde{b}_1 (\tilde{b}_1 \rightarrow t\tilde{\chi}^-_1)$ |
| $2b + E_T$                                 | $pp \rightarrow \tilde{t}_1\tilde{t}_1 (\tilde{t}_1 \rightarrow b\tilde{\chi}^+_1)$ |
|                                           | $pp \rightarrow \tilde{b}_1\tilde{b}_1 (\tilde{b}_1 \rightarrow b\tilde{\chi}^0_{1,2})$ |

TABLE I: The signals of the ATLAS stop/sbottom direct searches \cite{10,11}.
FIG. 3: Same as Fig. 2 but projected on the plane of stop mass versus neutralino mass. The samples denoted by bullets (red) are excluded by the ATLAS direct stop/sbottom search data at 95% CL.

Here $s_i$ is the signal events from our Monte Carlo simulation, and $n_i$ and $b_i$ are respectively the number of the observed and expected SM background events, which can be taken from the experimental papers. To account for the systematic uncertainty effect, we allow the number of background events in each channel to fluctuate: $b_i \to b_i(1 + \delta b_i)$. Following the analysis in Ref. 39, we convolve the Poisson distribution with a Gaussian weighting factor and then integrate over $b_i$:

$$\text{Pois}(n_i|b_i + s_i) \to \int d(\delta b_i) \text{Gaus}(\delta b_i, f_i^b) \text{Pois}(n_i|b_i(1 + \delta b_i) + s_i)$$

(15)

where $f_i^b$ is the width of the Gaussian distribution and is treated as the relative systematic uncertainty. Besides, we truncate the Gaussian integration in the case of the negative events number of background.
In Fig. 3 we show the constraints of the ATLAS stop/sbottom search data on the parameter space of natural SUSY. Generally, we can see that the stop mass can be more stringently constrained in case of \( m_{\tilde{t}_L} < m_{\tilde{t}_R} \) than in case of \( m_{\tilde{t}_L} > m_{\tilde{t}_R} \), which can be understood from Fig. 2 and Table I.

In the former case, since \( \tilde{t} \rightarrow t \tilde{\chi}^{0,1}_1 \) and \( \tilde{b} \rightarrow t \tilde{\chi}^{-1}_1 \) are the dominant decay modes for moderate stop/sbottom mass (\( m_{\tilde{t}_1} > 350 \) GeV), by using the ATLAS data of hadronic \( t\bar{t} + E_T \) and \( \ell + \text{jets} + E_T \), we can almost exclude \( 350 < m_{\tilde{t}_1} < 590 \) GeV and \( 350 < m_{\tilde{t}_1} < 605 \) GeV, respectively. But we should mention that since \( \tilde{t} \rightarrow t \tilde{\chi}^{0,1}_1 \) and \( \tilde{b} \rightarrow t \tilde{\chi}^{-1}_1 \) have the same signal, some samples with a heavier stop can also be excluded by these two channels. But in the latter case, the stop mass is hardly bounded by the stop searches due to the suppression of \( \tilde{t} \rightarrow t \tilde{\chi}^{0,1}_1 \) and \( \tilde{b} \rightarrow t \tilde{\chi}^{-1}_1 \). Besides, we note that the sbottom search data of \( 2b + E_T \) can give a complementary constraint on the stop mass, which excludes a light stop between 235–350 GeV in the former case and the exclusion limit can be up to 545 GeV in the latter case.

In Fig. 4 we combine the above exclusion limits from the three channels with \( CL_s \) method. It can be seen that the data can exclude at 95% CL a stop between 200–670 GeV for \( m_{\tilde{t}_L} < m_{\tilde{t}_R} \) and 250–600 GeV for \( m_{\tilde{t}_L} > m_{\tilde{t}_R} \). These combined limits are much stronger than the limits from single channel.

Note that since our analysis aim at the natural SUSY where the value of \( \mu \) is preferred to be small (usually below 200 GeV), our results are relevant for the low \( \mu \). If \( \mu \) becomes large (the lightest neutralino becomes heavy) but the stop mass is fixed, the small mass difference between them will make the visible decay products (jets or leptons) of the stop be soft. Thus the signal detection efficiency becomes lower so that our direct search limits will become weak. We checked and found that when \( m_{\tilde{t}_1} = 500 \) GeV, \( \mu > 300 \) GeV can escape the constraints considered in this work. Besides, we noticed that if \( \mu \) gets heavier, the stop should also become heavy to keep the neutralino as LSP, which will suppress the production rate of stop pair and escape our constraints.

The effects of \( \tan \beta \) on our results are shown in Fig. 5 in the case of \( m_{\tilde{t}_L} < m_{\tilde{t}_R} \). From this figure we see that the limits get weak for a large \( \tan \beta \). The reason is that in the case of \( m_{\tilde{t}_L} < m_{\tilde{t}_R} \) the decay width of \( \tilde{t}_1 \rightarrow \tilde{\chi}_1^{0,1} b \) (\( \tilde{t}_1 \rightarrow t \tilde{\chi}_1^{0} \)) is determined by \( y_b \sim 1/\cos \beta \) (\( y_t \sim 1/\sin \beta \)), and thus when \( \tan \beta \) gets large, the branching ratio of \( \tilde{t}_1 \rightarrow t \tilde{\chi}_1^{0} \) will be suppressed. Then the limits on the stop mass, which dominantly come from the decay \( \tilde{t}_1 \rightarrow t \tilde{\chi}_1^{0} \), will become weak.
In the case of $m_{\tilde{t}_L} > m_{\tilde{t}_R}$, our results are not sensitive to the value of $\tan \beta$ because in this case the decay widths of $\tilde{t}_1 \to \tilde{\chi}_1^+ b$ and $\tilde{t}_1 \to t \tilde{\chi}_1^0$ are both determined by $y_t$ and their branching ratios are not sensitive to $\tan \beta$.

In Fig. 6 we display the impact of the direct stop/sbottom searches on the stop sector. From the left panel we see that the two regions can be excluded by direct searches at 95% CL. The right panel shows that the range of $2 < X_t/M_s < 3$ can be excluded for $m_{\tilde{t}_1} < 600$ GeV at 95% CL.

![FIG. 4: Same as Fig. 3, but showing the combined exclusion limits.](image)

![FIG. 5: Same as Fig. 4, but showing the dependence on $\tan \beta$.](image)
Since the decay branching ratios of stop will be affected by the parameter $A_t$ through the mixing angle $\theta_t$, we let $A_t$ vary in our calculations to examine the its effect on the exclusion limit. However, when the stop mass $m_{\tilde{t}}$ is low (so that the LHC data can set limits), in order to get a 125 GeV SM-like Higgs we need a large $m_{\tilde{t}}$ in addition to a large $A_t$. Then from the formula $\sin(2\theta_t) = 2m_{\tilde{t}}X_t/(m^2_{\tilde{t}} - m^2_{\tilde{b}})$ where $X_t = A_t - \mu/\tan\beta$, we see that the value of $\sin(2\theta_t)$ is small and thus $\theta_t$ will be close to 0 or $\pm\pi/2$, which means that the stop is highly left-handed or right-handed. So the variation of $A_t$ can affect the stop mixing, but its effect is quite limited due to our requirement of 125 GeV Higgs. We checked numerically that the constraints are not sensitive to the value of $A_t$ in our case and mainly depend on the light stop scale and $\tan\beta$.

**IV. CONCLUSION**

We studied the constraints of the LHC search results on the stop mass in natural SUSY. Considering the constraints from the Higgs mass, B-physics and electroweak precision measurements, we scanned the parameter space of natural SUSY in the framework of MSSM, and then in the allowed parameter space we performed a Monte Carlo simulation for stop pair production followed by $\tilde{t}_1 \rightarrow t\chi^0_1$ or $\tilde{t}_1 \rightarrow b\chi^+_1$ and sbottom pair production followed by $\tilde{b}_1 \rightarrow b\chi^0_1$ or $\tilde{b}_1 \rightarrow t\chi^-_1$. Using the combined results of ATLAS with 20.1 fb$^{-1}$ from the search of $\ell + jets + \not{E}_T$, hadronic $t\bar{t} + \not{E}_T$ and $2b + \not{E}_T$, we found that a stop lighter than 600 GeV
can be excluded at 95% CL.

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Appendix A: Comparison of our simulation with the ATLAS results

In the following we present the comparison of our simulation with the ATLAS results. In Tables II, III and IV we present the results for \(2b + \not{E}_T, \ell + \text{jets} + \not{E}_T\) and hadronic \(t\bar{t} + \not{E}_T\), respectively.

| cuts | ATLAS | our simulation |
|------|-------|----------------|
| \(\not{E}_T > 150\) (GeV) | 270 | 239.27 |
| \(P_T(j_1), P_T(j_2), j_3\) (veto) | 110 | 91.85 |
| \(\Delta \phi_{\text{min}}(3)\) | 93 | 73 |
| \(\not{E}_T^{\text{miss}} / m_{\text{eff}}(j_1, j_2, j_3)\) and b-tag | 24 | 19.46 |
| \(m_{CT} > 100\) (GeV) | 22 | 17.27 |
TABLE III: Comparison of ATLAS and our simulation for $\ell + \text{jets} + \not\!E_T$ when $(\tilde{t}_1, \tilde{\chi}_1^0) = (650, 1)$ GeV

| cuts                                               | ATLAS    | our simulation |
|----------------------------------------------------|----------|----------------|
| No selection                                       | 500004.0 | 500004.0       |
| 1 $\mu$ and 4 jets (80,60,40,25)                   | 3704     | 3468           |
| $\geq 1$ b-tag in 4 leading jets                   | 3145.2   | 3089           |
| $E_T^{\text{miss}} > 100$ (GeV)                    | 2930     | 2838           |
| $E_T^{\text{miss}} / \sqrt{H_T} > 5$              | 2844.2   | 2757           |
| $\Delta\phi(\text{jet}, E_T^{\text{miss}}) > 0.8$ | 2649     | 2488           |
| $m_T > 200$ (GeV)                                  | 2210.6   | 2016           |
| $m_T > 140$ (GeV)                                  | 1474.9   | 1203           |

TABLE IV: Comparison of ATLAS and our simulation for hadronic $t\bar{t} + \not\!E_T$ when $(\tilde{t}_1, \tilde{\chi}_1^0) = (600, 0)$ GeV

| cuts                                               | ATLAS    | our simulation |
|----------------------------------------------------|----------|----------------|
| No selection                                       | 507.5    | 507.5          |
| $e/\mu$ veto                                       |          |                |
| $E_T^{\text{miss}} > 130$ (GeV)                    | 270.1    | 303.8          |
| Jet multiplicity and $p_T$                         | 92.2     | 105.1          |
| $E_T^{\text{track}} > 30$ (GeV)                    |          |                |
| $\Delta\phi(\text{jet}, E_T^{\text{miss}}) > \pi/5$ | 72       | 82.5           |
| $\Delta\phi(E_T^{\text{miss}}, E_T^{\text{miss,track}} < \pi/3$ | | |
| tau veto and b-tag                                 | 31.5     | 33.06          |
| $m_T(b\text{-jet}, E_T^{\text{miss}}) > 175$ (GeV) | 23.6     | 19.3           |
| $80$ (GeV) $< m_{jjj}^{0.1} < 270$ (GeV)           | 11.9     | 10.14          |
| $E_T > 150$ (GeV)                                  | 11.8     | 9.89           |
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