Constructal approach to bio-engineering: the ocular anterior chamber temperature

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The aim of this work was to analyse the pressure inside the eye’s anterior chamber, named intraocular pressure (IOP), in relation to the biomechanical properties of corneas. The approach used was based on the constructal law, recently introduced in vision analysis. Results were expressed as the relation between the temperature of the ocular anterior chamber and the biomechanical properties of the cornea. The IOP, the elastic properties of the cornea, and the related refractive properties of the eye were demonstrated to be dependent on the temperature of the ocular anterior chamber. These results could lead to new perspectives for experimental analysis of the IOP in relation to the properties of the cornea.

In vision processing, images flow from the external environment to the brain. The information processed in this complex system during viewing was developed into a morphological network that can be modelled by the constructal law. Indeed, the brain architecture is closely linked to the information flow system, which is explained by stating that “the eyes scan the viewing area in the shortest time”1. Moreover, it has been emphasized that “The visual sensors and nerves in the retina are configured in the same way, as dendrites, in order to provide greater access between one surface (the retina) and one point (the optic nerve)”1.

This approach represents a new interesting method of analysing the complex systems that constitute vision and eyes because bio-engineering combines physical, chemical and applied mathematical results to study biological phenomena, and usually relates them to mechanical, electronic or information sciences. On the other hand, constructal law analyses the flows between the system and its environment, introducing a new viewpoint in engineering sciences2. Recently, by introducing this new basic and fundamental position into biochemical thermodynamics3–6, a biochemical engineering thermodynamic approach7,8 has been developed for complex biological systems, based on the analysis of interactions between a particular biological system and its environment. The result is a comprehensive understanding of the biophysical, biochemical and physiological processes in specific systems.

Here, we extend this approach to analysing the intraocular pressure (IOP), which is the fluid pressure inside the eye. Progressive loss-of-vision related to any IOP disorder is known as glaucoma, and it represents one of the major causes of blindness. In addition, IOP measurements are one of the most important medical parameters in postoperative evaluation for corneal, lenticular and vitreoretinal diseases.

There is a large amount of experimental evidence regarding the relevance of the central corneal thickness (CCT) in the measurement (tonometry) of the IOP9,10 and, therefore, mathematical models to study biological phenomena, and usually relates them to mechanical, electronic or information sciences. Indeed, biomechanical analyses of the physical properties of the eye, in particular the cornea, are too complex to obtain a general mechanical model for linking the tissue morphology to their elastic properties and to the flows between the eye and its external environment11. The cornea tissue is characterized by the properties of the soft material, in particular12–23.
1. Heterogeneity in the central-to-peripheral, and anterior-to-posterior dimensions\cite{12};
2. Near incompressibility, due to the large amount of water and collagen fibres, with a consequent Poisson’s ratio of the cornea of about\cite{13} 0.5;
3. Non-linear constitutive behaviour in relation to the IOP variation\cite{14};
4. Viscoelastic and creep behaviour observed in cyclic tests\cite{15};
5. Structural anisotropy generated by the oriented collagen fibrils\cite{16}.

Furthermore, biomechanical problems of the cornea are fundamental in certain diseases, such as\cite{17}

1. Keratoconus, in relation to loss-of–rigidity in the cornea, and
2. Cornea ectasia after cornea refractive surgery, in relation to progressive cornea deformation due to impairment of the stroma.

In recent decades, measuring the cornea temperature has been shown to be indicative for many applications in diagnosing ocular disease\cite{24}. On the other hand, there are plenty of models for the study of the cornea elastic properties and heat exchange, but there isn’t a general analytical models to link the cornea thermo–elastic properties with anterior chamber thermal behaviour. This correlation is in fact very important as the flow of aqueous humour in the anterior chamber is crucial for maintaining IOP, along with the shape and stability of the visual system, the diffusion of nutrients and the removal of metabolic waste\cite{25}. The temperature gradient between the anterior and posterior surfaces of the anterior chamber causes buoyancy, which is the principal mechanism that causes anterior chamber flows\cite{25–30}. In this context, we highlight that temperature is one of the principal regulators of tissue metabolism, and there is a continuous interest for analysing temperature in the study of ocular physiology and pathology\cite{21}. However, to date there are no theoretical models able to support physicians in their analysis\cite{21}.

Due to the theoretical difficulties in obtaining general results, a new approach can be adopted in order to analyse the properties of the cornea and the ocular anterior chamber in relation to IOP studies. To do so, we consider that flows of water (or in general, of liquids) constitute the IOP and, therefore, introducing the constructal law in the context of ophthalmological analysis of IOP is logical and interesting.

Consequently, in this investigation, we aimed to link constructal law to irreversible bioengineering thermodynamics in order to obtain a new approach for studying IOP, for analysing the relation between the cornea properties and the risk of glaucoma in hypertensive patients.

**Results**

The constructal law is applied by analysing the effects of liquid flows in the ocular anterior chamber. Results are expressed as a relation between the temperature of the ocular anterior chamber and the environmental temperature.

Figure 1 represents the temperature of water inside the anterior chamber (a) and cornea temperature (b) in relation to the variation of the environmental temperature. We highlight that inside water temperature and cornea temperature growth with the growth of the environmental temperature. Figure 2 represents the cornea elastic potential energy in relation to cornea temperature. We highlight that the elastic potential energy decrease with the cornea temperature growth. Our results can be compared with the results obtained in refs 19,21. Our results agree with recent studies on humans\cite{28–30}. Indeed, they highlighted that eyes with ischemic central venous retinal occlusion (determined by high pressure) have lower ocular surface temperature than non-ischemic eyes. It agrees with our result because the cornea potential energy is the work done by the border of the eye, and its magnitude is proportional to the magnitude of the intraocular pressure which causes the work against this surface. Consequently, lower the temperature greater the corneal potential energy and greater the intraocular pressure, with consequent ischemic consequences on the optic nerve.

**Figure 1. Temperature of the ocular anterior chamber and the cornea.** Temperature of the ocular anterior chamber (a) and the cornea (b) were evaluated by using the equations (6 and 7) in relation to the variation of external environmental temperature.
They agree with the experimental results summarized in the literature. It can be highlighted that the cornea temperature depends more on the environmental temperature than the anterior chamber.

Finally, we evaluated the elastic work (potential energy variation) of the cornea in relation to the cornea temperature. The work done by the cornea was found to decrease with the temperature. However, the cornea temperature is determined both by the environmental temperature and by the anterior chamber temperature. Therefore, there is a relation between the elastic work carried out by the cornea against the anterior chamber pressure and the anterior chamber temperature, consequently, there is a relation between the cornea thickness and the IOP. Our approach allows us to obtain this relation.

From equation (10), it can be highlighted that the difference between the inflow and outflow of liquids is the main cause of the variation in the elastic properties of the cornea and of the related IOP.

Discussion

Glaucoma is a very serious optic neuropathy in which the destruction of ganglion cells and fibres determines an irreversible loss of visual field, and represents a cause of blindness. Controlling the IOP prevents patients from sustaining damage due to glaucoma and avoids blindness. Conversely, increasing IOP represents a primary risk factor for glaucoma development. Thermography has been used in the study of vascular factors in the physiopathology of glaucoma, revealing that ocular surface temperature can be used as an indicator of impaired retrobulbar haemodynamics in glaucoma studies.

The cornea is the primary ocular refractive structure in the eye composed of five layers (epithelium, Bowman’s layer, stroma, Descemet’s membrane, and endothelium). It has a radius of 10–11 mm and a thickness of 0.5 mm. The cornea exchanges heat with the environment and with the anterior chamber; consequently, its surface temperature results as being underlying in maintaining the temperature of the anterior chamber constant. The temperature of the cornea can be obtained by considering the conductive heat transfer across the cornea and, in this way, a relation between the cornea temperature and the anterior chamber is obtained. Moreover, its elastic properties affect the value of the IOP; indeed, in 1957, Goldmann and Schmidt introduced the hypothesis that the IOP is underestimated in patients with thin corneas, while it is overestimated in patients with thick corneas. A correlation between the cornea thickness and the IOP has been experimentally verified, and can be attributed to the fact that the IOP is the sum of the effects of:

1. The swelling pressure (SP), the repulsion caused by the negatively charged stromal glycosaminoglycans, and
2. The imbibition pressure (IP), the negative pressure that causes the fluid inflow into the cornea (\(IOP = SP + IP\)).

From our results, we can state that:

1. There is a relation between the temperature of the ocular anterior chamber and the IOP;
2. There is a relation between the cornea temperature and the temperature of the ocular anterior chamber;
3. There is a relation between the cornea temperature and its elastic behaviour;
4. There is a relation between the IOP and the cornea thickness, which can be evaluated by measuring the ocular anterior temperature.

The first principle of thermodynamics can be introduced to evaluate the work done by the anterior chamber against the internal cornea wall. The temperature of the aqueous humour is related to the difference between the heat dissipated across the cornea and the heat generated by metabolic activities and the vascular supply to the anterior chamber. Thus, temperature plays a role in regulating the aqueous humour secretion, excretion, and flow dynamics, with consequences on the IOP regulation and the relative diseases, such as glaucoma. Moreover, the correlation between the anterior chamber temperature and the cornea temperature can be utilised for analysing the tear film evaporation and its relation to the environmental conditions. Therefore, it can be assumed that the transient receptor potential channel isoforms may play a crucial role in the control of aqueous humour dynamics, as suggested by Fabiani. As such, temperature can be introduced as a new additional target in the control of glaucoma progression in ocular hypertensive patients. It should be highlighted that there is a trend for ocular temperature to decrease with age and it is therefore important to introduce these new approaches by
evaluating individual patients with relation to his/her personal evolution. Finally, a relevant relationship between cornea elastic properties, refractive errors, and anterior chamber properties has been experimentally highlighted29, confirming our theoretical results: a recent study on humans highlighted that eyes with ischemic central venous retinal occlusion (CRVO) have lower ocular surface temperature than non-ischemic eyes30. Last, Galassi et al. has defined ocular surface temperature as a marker of impaired retrobulbar hemodynamics in patient with glaucoma38.

So, from the constructal law, we can introduce the analysis of liquid fluxes in the ocular anterior chamber. Variation of the mass flows in the anterior chamber cause an alteration in IOP and, consequently, in the elastic properties of the cornea. However, the cornea properties affect the refractive properties of the eye and, as a result, a variation in IOP could also be assessed by evaluating the vision itself. Indeed, IOP depends only on the flows of aqueous humour which is a balance between secretion and excretion. Three mechanisms are involved in the aqueous humour formation: diffusion, ultrafiltration, and active secretion. Constructal law is a physical approach based on the analysis of the flows. It is a new approach introduced in thermodynamics by Adrian Bejan in order to explain optimal shapes of natural structures31. This law is finding its applications from engineering to economics, from physics to biology, from hydraulics to geology, from urban designing to physiology, etc.32-37. The constructal law describes how Nature and engineers “design” a system, so it is very useful to understand the bases of the biosystems and their interaction with the environment through flows.

In conclusion, there exists a correlation between IOP and temperature. Temperature can be measured by non-contact measurements systems. This characteristic is interesting to design non contact tonometers for future home patients controls and related personalized therapies.

Methods
In order to extend a constructal approach from the analysis of vision to the analysis of the eyes, we considered that the flows related to IOP are water inflows and outflows between the ocular anterior chamber and blood vessels. Therefore, considering the eye as an open system in relation to the body, we apply the first law of thermodynamics38:

$$Q - W = \frac{d}{dt} \left[ U + p_0 V + \int_{CV} \rho (c_v + c_p) dV \right] + m_{\text{out}} (h + c_v + c_p)_{\text{out}} - m_{\text{in}} (h + c_v + c_p)_{\text{in}}$$

where \(Q\) is the heat power exchanged between the cornea and the external environment, \(W\) is the mechanical power carried out by the tissue in relation to the pressure and elastic properties of the cornea, \(U\) is the internal energy, \(p_0\) is the external environmental pressure, \(V\) is the volume of the anterior chamber, \(\rho\) is the water density, \(c\) is the specific energy, \(k\) stands for kinetic, \(p\) as a subscript means potential, \(h\) is the specific enthalpy of the water, \(in\) means inflow, \(out\) means outflow, and \(CV\) means control volume. The kinetic energy and the potential energy are so small that they can be considered null, and we analysed the behaviour of the eye during the time of observation, so that we integrated time, obtaining:

$$Q = -m_w c_v (T_w - T_0)$$

obtaining:

$$-W = (m_{\text{out}} - m_{\text{in}}) c_v T_w + p_0 \Delta V + m_{\text{out}} c_p T_w - m_{\text{in}} c_p T_{\text{in}} + m_w c_v (T_w - T_0)$$

Then, we can evaluate the work carried out by the water against the external surface of the anterior chamber as38:

$$W = -V \Delta \text{IOP}$$

and the ocular anterior chamber temperature results can be obtained:

$$T_w = \frac{V}{c_v (2m_{\text{out}} - m_{\text{in}} + m_w)} \Delta \text{IOP} - \frac{\text{IOP}}{c_w (2m_{\text{out}} - m_{\text{in}} + m_w)} \Delta V + \frac{m_{\text{out}} T_w + m_{\text{in}} T_{\text{in}}}{2m_{\text{out}} - m_{\text{in}} + m_w}$$

where \(c_v = c_p = c_w\) is the specific heat of the liquid water. In an eye without any pressure diseases \(m_{\text{out}} \approx m_{\text{in}}, p_0 \approx \text{IOP}\) as it represents the pressure of the interior chamber against the elasticity of the cornea back wall.

Starting from this result, we can consider that the anterior chamber exchanges heat through the cornea surface. The heat transfer mechanisms are the conduction across the cornea length, and the convection with the environmental air on the cornea external surface. So, the value of the cornea temperature \(T_c\) can be obtained by the usual heat transfer approach38, as follows:

$$T_c = T_w - \frac{T_c - T_0}{\frac{1}{\alpha} + \frac{1}{\lambda}} \cdot s$$
where $s$ is the mean corneal thickness (0.5 mm), $\lambda$ is the cornea conductivity (0.6 W m$^{-1}$ K$^{-1}$) and $\alpha$ is the convective heat transfer coefficient (50 W m$^{-2}$ K$^{-1}$). The results obtained are represented in Fig. 1. It should be noted that the cornea temperature is more affected by the environmental temperature and that the cornea temperature is crucial in relation to the variation of the anterior chamber temperature. The data obtained agrees with the data in the literature$^{18–21}$ as discussed in the previous section, with an error of less than 1% (see refs 19, 21). The time of observation considered is greater than the thermal transient, evaluated$^{19}$ in 5000 s.

Now considering the extended Bernoulli’s equation$^{36}$.

$$W = \int pdV - p_0 \Delta V - W_L - \Delta E_k - \Delta E_p$$

(8)

where $W_L$ is the work lost for irreversibility, $E_k$ is the kinetic energy and $E_p$ is the cornea elastic potential energy, and introducing this into the relation (4) it follows that the elastic potential variation of the cornea results as:

$$\Delta E_p = (m_{out} - m_{in})c_w T_w + (m_{out}c_w T_w - m_{in}c_w T_{in} + m_sc_w(T_w - T_{in})$$

(9)

This result is represented in Fig. 2. The shape has been obtained considering the kinetic energy and the work lost for irreversibility as being null. It should be emphasized that the cornea elastic work (variation of the elastic potential energy) depends on the temperature of the cornea.

Finally, considering the relation (10) and the relation (6) it follows that

$$\Delta E_p = Y \cdot s = (2m_{out} - m_{in})c_w \left[\frac{\Delta (V \cdot IOP)}{c_w(2m_{out} - m_{in} + m_{in})} + \frac{m_{in}T_w + m_sc_wT_{in}}{2m_{out} - m_{in} + m_w} - m_{in}c_wT_{in}\right] + m_sc_w \left[\frac{\Delta (V \cdot IOP)}{c_w(2m_{out} - m_{in} + m_{in})} + \frac{m_wT_{out} + m_sc_wT_{out}}{2m_{out} - m_{in} + m_w} - T_{in}\right]$$

(10)

where $Y$ is the Young modulus and $s$ is the cornea thickness.

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Author Contributions
U.L. developed the irreversible biochemical engineering thermodynamic model and introduced the constructal law as the basis of analysis of the ocular properties. A.P. developed the biomedical considerations. D.D. and M.R.A. developed the ophthalmologic considerations. G.G. and E.M. analysed the data. All authors contributed to the main manuscript text and reviewed the manuscript.

Additional Information
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