Towards Quantum Enigma Cipher II
-A protocol based on quantum illumination-

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Abstract—This research note II introduces a way to understand a basic concept of the quantum enigma cipher. The conventional cipher is designed by a mathematical algorithm and its security is evaluated by the complexity of the algorithm in security analysis and ability of computers. This kind of cipher can be decrypted with probability one in principle by the Brute force attack in which an eavesdropper tries all the possible keys based on the correct ciphertext and some known plaintext. A cipher with quantum effects in physical layer may protect the system from the Brute force attack by means of the quantum no cloning theorem and randomizations based on quantum noise effect. The randomizations for the ciphertext which is the output from the mathematical encryption box is crucial to realize a quantum enigma cipher. Especially, by randomizations, it is necessary to make a substantial difference in accuracy of ciphertext in eavesdropper’s observation and legitimate user’s observation. The quantum illumination protocol can make a difference in performance of the legitimate’s receiver and the eavesdropper’s receiver. This difference is due to differences in ability of the legitimate’s receiver with entanglement and the eavesdropper’s receiver without entanglement. It is shown in this note that the quantum illumination can be employed as an element of the most simple quantum enigma cipher.

I. INTRODUCTION

The general network systems need to be protected from interception by unauthorized parties. The most serious attack is “Cyber attack against Layer-1 (physical layer such as optical communication line)”, because technologies of coupler for tapping have been developed by several institutes [1]. In addition, there are many optical monitor ports for network maintenance. In fact physical layer of high speed data link is a defenseless. To date, that protection has been provided by classical encryption systems. However, such technologies cannot ensure the provable security, and also the eavesdropper can obtain the correct ciphertext of mathematical cipher for payload at Layer-2, and she can store it in memory devices. Thus, we cannot rule out the possibility that the cipher may be decrypted by future technology.

The best way to protect high speed data is to physically randomize signals as the ciphertext of the mathematical encryption. This is called physical random cipher. The most important feature of this physical random cipher is that the eavesdropper cannot get the correct ciphertext of mathematical encryption box, for example a stream cipher by PRNG (pseudo random number generator), from communication lines, while the legitimate user can get it based on a knowledge of secret key of PRNG. Thus, the ciphertext: \( Y^B(C) \) as the signal of the legitimate user and the ciphertext: \( Y^E(C) \) as the signal of the eavesdropper may be different as \( Y^B(C) \neq Y^E(C) \).

Along with this concept, Quantum Enigma Cipher allows a secure high speed data transmission by means of the quantum noise randomization by a mathematical encryption box and signal modulation systems, or by an integration of a mathematical encryption box and a physical encryption box [2]. When we consider how to realize such a system, we have to take into account the following requirements on the encryption system in the real world:

Requirement of specifications:
(1) Data-speed: 1 Gbit/sec \( \sim \) 100 Gbit/sec
(2) Distance: 1000 Km \( \sim \) 10000 Km
(3) Encryption scheme: Symmetric Key Cipher
(4) Security: Provably secure, Secure against Brute force attack (exhaustive search trial for secret key) by means of computer and also physical devices.

Recently, MIT groups claimed to be capable of their quantum illumination scheme to provide ultra-broadband secured communication [3,4]. The principle is that the quantum illumination protocol can produce the difference between Alice’s error performance and Eve’s error performance. We can adopt such a scheme in quantum enigma cipher as a physical randomization technique. The author believes that this is the most appropriate application of the quantum illumination. In the following sections, we will discuss the reason and method to realize quantum enigma cipher based on quantum illumination.

II. SECURITY OF SYMMETRIC KEY CIPHER INCLUDING ONE TIME PAD

A. Model

Let us describe a standard symmetric key encryption. A general symmetric key encryption \( \Lambda \) can be given by

\[
\Lambda = ([P_K], Enc, Dec)
\]

where \([P_K]\) is key generation algorithm and it provides key sequence \( K \in K \) depending on the probability \( P_K \). Enc is an encryption algorithm which generates...
ciphertext $C = Enc(K, M)$ where $M$ is plaintext. $Dec$ is a decryption algorithm which produces plaintext $M = Dec(K, C)$.

B. Security criterion

When $A$ cannot be decrypted by means of computational resource, its security is evaluated by “Guessing probability”\[5,6\].

(i) Ciphertext only attack on data:

$$P_{G}(M) = \max_{M \in \mathcal{M}} P(M|C)$$ \hspace{1cm} (2)

(ii) Ciphertext only attack on key:

$$P_{G}(K) = \max_{K \in \mathcal{K}} P(K|C)$$ \hspace{1cm} (3)

On the other hand, when some plaintext $M_{k}$ and ciphertext corresponding to them are known, it is called known plaintext attack. It is easy to generalize the above formula as follows:

(iii) Known plaintext attack on data:

$$P_{G_{k}}(M) = \max_{M \in \mathcal{M}} P(M|C, M_{k})$$ \hspace{1cm} (4)

(iv) Known plaintext attack on key:

$$P_{G_{k}}(K) = \max_{K \in \mathcal{K}} P(K|C, M_{k})$$ \hspace{1cm} (5)

These are sometimes called maximum “a posteriori probability” guessing. If one needs an average, then one can define average guessing probability as follows:

$$P_{G}(M) = \sum_{C \in \mathcal{C}} P(C) \max_{M \in \mathcal{M}} P(M|C)$$ \hspace{1cm} (6)

C. Security of ideal one time pad

When the distribution $P_{K}$ is uniform, the one time pad has the perfect secrecy such that

$$P_G(M) = \max_{M \in \mathcal{M}} P(M|C) = P(M)$$ \hspace{1cm} (7)

However, even if the system has the perfect secrecy, it does not mean “secure” against known plaintext attack on data when data is a language such as English. That is,

[The perfect secrecy means secure against ciphertext only attack, and it does not imply the security against “known plaintext attack and falsification attack”.]

Thus, the term of “unconditional security” is misleading. Let us show an example. The eavesdropper can get the correct ciphertext of the length $|K|$ bits, and she can launch the Brute force attack. The decrypted data sequences of the length $|K|$ bits give all combination of English alphabet (ASCII code) of length $|K|$ bits. These include a large number of correct English words such as “orange, signal, cipher, and so on”. When the attack is ciphertext only attack, she cannot decide which word is the real plaintext. However, if she knows the first alphabet “o” as the known plaintext attack, the correct word may be “orange”. Thus, the guessing probability may become very large value.

D. Security of one time pad forwarded by QKD

The quantum key distribution does not provide the perfectly uniform distribution for key sequence $K_{G}$ against an eavesdropper. In fact, the average guessing probability is given by Portman and Renner[7] as follows:

$$\hat{P}_G(K_{G}) \leq \frac{1}{2^{|K_{G}|}} + d$$ \hspace{1cm} (8)

where $d$ is the trace distance in QKD protocol. Thus, the one time pad forwarded by QKD is non ideal one time pad which is encrypted by key sequence with non uniform distribution. That is,

$$\Lambda = ([P_{K} \neq \text{ideal}, Enc, Dec], P_{K} \neq \frac{1}{2^{|K_{G}|}})$$ \hspace{1cm} (9)

If the value of the trace distance is very large in comparison with $\frac{1}{2^{K_{G}}}$, the guessing probability is very large. So such a one time pad may be decrypted easily[5,6].

In addition, QKD needs an initial secret key for the authentication before the legitimate users start the QKD protocol. This is the same situation as the conventional symmetric cipher in which the key is for initial seed key for PRNG. Thus, we cannot start cryptographic action without certain initial secret key, except for the conventional public key encryption.

III. DEFINITION AND SECURITY OF QUANTUM ENIGMA CIPHER

A. Definition

Let us describe here the ideal quantum enigma cipher system. The quantum enigma cipher consists of an integration of mathematical encryption box and physical randomization for ciphertext of mathematical encryption box [2]. The mathematical encryption box has a secret key of the length $|K_{s}|$ bits and PRNG for expansion of the secret key. The physical encryption box has a mechanism to create ciphertext as signal and it has a function to induces an error when the eavesdropper receives the ciphertext as signal. Consequently different ciphertext sequences are observed in the legitimate’s receiver and the eavesdropper’s receiver, respectively. A requirement for the physical randomization is

$$P_{s}(Eve) >> P_{s}(Bob \ or \ Alice)$$ \hspace{1cm} (10)

This means that the error performance $P_{s}$ of the eavesdropper becomes worse than that of the legitimate user,
when they observe the ciphertext as signal in communication lines. We can consider many schemes to realize the above condition based on several quantum effects such as quantum noise, entanglement. But the system has to satisfy the conditions described in the introduction.

B. Security

The conventional symmetric key cipher produces the ciphertext of length at most $2|K_s|$ bits. Because the key length is $|K_s|$ bits, when the eavesdropper gets the known plaintext of the length $|K_s|$ bits and ciphertext corresponding to them, she can pin down the secret key by the Brute force attack (trying $2|K_s|$ key candidates). That is, the guessing probability is one. In addition, the sequence of the ciphertext has certain correlation because of the structure of PRNG. So the eavesdropper can investigate several mathematical algorithms to estimate the secret key.

In the ideal quantum enigma cipher, the eavesdropper’s observation of the ciphertext as signal in communication lines suffers error completely, while the legitimate user does not. So the legitimate user can decrypt by the secret key, but the eavesdropper does not even if she gets the secret key after her observation of ciphertext as signal. Thus, the guessing probability is

$$P_{G}(K_s) = 2^{-|K_s|} \tag{11}$$

even if she collects the ciphertext of $2|K_s|$ bits. This means an immunity against the Brute force attack by computers. On the other hand, the quantum no cloning theorem may protect a physical Brute force attack by cloning whole quantum states, because a set of quantum states for the quantum enigma cipher are designed by non-orthogonal state with very close signal distance each other.

IV. APPLICATION OF QUANTUM ILLUMINATION

It is not clear whether the quantum illumination protocol provides the ideal difference between the correctness of the ciphertext or not:

$$\eta_{ideal} = \frac{P_{G}(Eve)}{P_{G}(Bob)}(K_s) = P_{G}(Eve)(K_s) = 2^{-|K_s|} \tag{12}$$

However, it may be one of the quantum methods to create the different correctness of the ciphertext as signal according to [3,4]. If it is so, the application of quantum illumination is very easy.

(1) Alice generates entangled state, and sends the signal mode to Bob.

(2) Bob prepares a mathematical encryption box to encrypt the data sequence and modulates the received light by means of BPSK, but the signal for the modulator is the ciphertext from the mathematical encryption box.

(3) Bob employs the conventional optical amplifier to mask the ciphertext signal by the spontaneous emission noise from the amplifier. Then he returns optical signal to Alice.

(4) Alice can recover the ciphertext signal from the masking by noise by means of entanglement effect at her receiver. But Eve’s receiver suffers the error because she cannot use the entanglement.

So far, the quantum illumination protocol has been proposed for a direct encryption to plaintext, and for key generation [3,4]. However, this is not a good idea, because it is difficult to guarantee its security. It should be used as a physical randomization technique. The scheme introduced here is an example based on the most simple cascade cipher of the mathematical encryption box and the physical randomization. Even so, the structure of security analysis is drastically changed. First we need an optimization as follows:

$$\eta_{error} = \max_{\Lambda_{QI}} \frac{P_e(Eve)}{P_e(Alice)} \tag{13}$$

where $\Lambda_{QI}$ is a set of quantum illumination with several physical parameters. According to [4],

$$P_e(Eve) = \exp(-4W \kappa_{GB} N_S^2 / RN_B) / 2 \tag{14}$$

$$P_e(Alice) = \exp(-4W \kappa_{GB} N_S / RN_B) / 2 \tag{15}$$

Although we need complicated analysis to derive the guessing probability of the secret key of the mathematical encryption box based on the above under the unconditional setting, it may be expected to perform well.

V. FOR FUTURE

We have given an example of the concept of the quantum enigma cipher by using quantum illumination technique. In the sense of theoretical cryptology, such a cascade cipher would not be attractive. The real quantum enigma cipher requires the emergence of the additional enhancement for the security or the function by integrating the mathematical encryption box and the physical randomization such as the triple DES in the conventional cipher. The quantum noise randomized stream cipher $\alpha/\eta[8,9]$ and Y-00 [10,11] is a random cipher along with this concept. However, the masking is very small in the real setting, so they need additional randomization methods [12] or a new technique. A key concept is how to protect a secret key of the mathematical encryption box by the law of quantum mechanics. The author is expecting a good proposal.

VI. CONCLUSION

Quantum key distribution has only just one of the functions of cryptology that provide secret key sequence for realizing one time pad. As described in this note, the one time pad is not a new concept in cryptology, but quantum enigma cipher is indeed a new concept in cryptology. It was claimed that the quantum illumination
may provide G bit/sec rate. But the direct encryption and also the one time pad based on it are not an attractive scheme for the real world. Thus it is preferable to adopt as a physical randomization technique to the quantum enigma cipher.

The purpose of this note is to introduce the concept of the quantum enigma cipher using the quantum illumination. The author would like to emphasize that there are many ways to realize quantum enigma cipher by applying the quantum physics, but he does not know how to establish the ideal system design to provide the different performance from simple cascade effect. This note may give a hint.

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