Analysis of phase coherence in fully developed atmospheric turbulence: Amazon forest canopy

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Abstract. In a recent paper (Koga et al., 2007) it was shown that the intermittent nature of solar wind turbulence can be characterized by kurtosis and phase coherence index. In this paper, we apply these two nonlinear time series techniques to characterize the intermittent nature of atmospheric turbulence above and within the Amazon forest canopy using the day-time data of temperature and vertical wind velocity measured by a micrometeorological tower at two different heights. By applying kurtosis and phase coherence index to quantify the degree of phase coherence, we identify an enhanced scalar-velocity similarity for in-canopy turbulence compared to the above-canopy turbulence, during the interval of data analysis.

1 Introduction

Amazon rain forest plays a key role in the regional and global climate dynamics. One important problem for understanding the vegetation-atmosphere interactions in Amazonia is the turbulent exchange of scalar and momentum in the atmospheric boundary layer - above and within the forest canopy.

Atmospheric turbulence in the Amazon forest has been investigated extensively. For example, Fitzjarrald et al. (1990) performed detailed observations of turbulence just above and below the crown of an Amazon forest during the wet season. This analysis shows that the forest canopy removes high-frequency turbulent fluctuations while passing lower frequencies. A study of CO\textsubscript{2} concentration was made by Sternberg et al. (1997) in two different forests in the Amazon basin during the dry season, one site characterized by a closed canopy structure in which turbulent mixing is minimized and another site characterized by an open canopy structure in which the turbulent mixing is maximized. This analysis shows that the respiratory CO\textsubscript{2} recycling in the closed canopy forest with lower wind speeds is occurring to a greater extent than the open canopy forest with higher wind speeds. The vertical dispersion of trace gases using a Lagrangian approach was analyzed by Simon et al. (2005) based on in-canopy turbulence data collected at Jaru and Cuieras Reserves. This study indicates that for day-time conditions when there is an efficient turbulent mixing in the upper canopy and profile gradients are small, the radon-222 source/sink distributions show a high sensitivity to small measurement errors and the CO\textsubscript{2} and H\textsubscript{2}O fluxes show a reasonable agreement with the eddy covariance measurements made above the forest canopy, which is not the case for night-time conditions when the CO\textsubscript{2} profile gradients in the upper canopy are large due to reduced turbulent mixing.

The intermittent characteristics of atmospheric turbulence above and within a forest canopy has been discussed by a number of papers. For example, a review of turbulence in plant canopies was written by Finnigan (2000) who noted an upsurge of interest in canopy turbulence sparked by the need to understand global biochemical cycles and their role in climate change. An analysis of fine-scale canopy turbulence in an Amazon forest based on the generalized Tsallis’ thermostatistics theory was performed by Bolzan et al. (2002). This investigation shows that the entropy parameter $q$ from Tsallis’ non-extensive statistics, that controls the shape of the probability density function (PDF) of velocity
and temperature differences, can be used to quantify the intermittency buildup in atmospheric turbulent flows. Ramos et al. (2004) extended the study of Bolzan et al. (2002) to investigate how the entropy parameter $q$ varies from above to within the forest canopy, or when the atmosphere changes from day/unstable to night/stable conditions. In addition, it is shown that large-scale, ramp-like, coherent structures in the temperature fields affect the properties of the inertial subrange resulting in an increase of the temperature kurtosis above the canopy. Using time series of turbulent velocity and scalar concentration collected in the atmosphere above a temperate pine forest, Katul et al. (2006) demonstrated that Tsallis’ non-extensive thermostatistics provides a unifying framework to study two inter-connected problems: dissimilarity between scalars and velocity statistics within the inertial subrange and contamination of internal intermittency by external factors. This work indicates that the dissimilarity in statistics between velocity and scalars within the inertial subrange is strongly dependent on external intermittency. Thomas et al. (2006) applied a Doppler-Sodar to observe coherent structures in the roughness sublayer above forest canopy, and found that the turbulent flow is a superposition of dynamic Kelvin-Helmholtz instabilities and convective mixing.

In analytic modeling and numerical simulations of intermittent turbulence based on a set of deterministic equations, in the absence of noise, it is naturally expected that the departure from Gaussianity is due to phase coherence related to nonlinear interactions (Frisch, 1995). In contrast, the observational data of atmospheric turbulence is an admixture of deterministic signal and stochastic noise. In such case, a demonstration of finite phase coherence is required to ascertain the nonlinear origin of non-Gaussian fluctuations. Recently, a phase coherence technique based on surrogate data has been developed for nonlinear space data analysis (Hada et al., 2003; Nariyuki and Hada, 2006; Koga et al., 2008). The link between phase coherence, non-Gaussianity and intermittent turbulence was established by Koga et al. (2007), based on GEOTAIL magnetic field data upstream and downstream of the Earth’s bow shock. The aim of this paper is to apply the kurtosis (fourth-order structure function) and phase coherence techniques to determine the intermittent nature of day-time atmospheric turbulence above and within the Amazon forest canopy. In particular, we show that both techniques are capable of characterizing the dissimilarity of scalar and velocity in above-canopy and in-canopy atmospheric turbulence.

2 Amazon forest canopy data

A major atmospheric mesoscale campaign during the wet season of the Large-Scale Biosphere-Atmosphere Experiment in Amazonia (LBA) was carried out in January–March 1999 (Silva Dias et al., 2002). LBA is an international project led by Brazil designed to study: 1) the climatological, ecological, biogeochemical, and hydrological functions of the Amazon region, 2) the impact of land uses caused by deforestation, and 3) the interactions between Amazonia and the Earth system. As part of this campaign, a micrometeorological tower was set up in a southwest Amazon basin at the Biological Reserve of Jaru (Rebio Jaru: $10^\circ04^\primeS$, $61^\circ56^\primeW$) in Rondônia State of Brazil; with instruments located at two different heights: above-canopy at 66 m and inside-canopy at 21 m, to make simultaneous measurements of eddy covariance and vertical profiles of air temperature, wind velocity, radiation and humidity. Three-dimensional wind velocity and air temperature measurements were made at a sampling rate of 60 Hz, using sonic anemometers and thermometers.

In this paper we investigate the atmospheric turbulence data taken from noon to 12:30 on Julian Day 068, when the forest crown is heated by the solar radiation. A dataset of 108 000 points for temperature and vertical velocity is used for this analysis. During this period the top of the canopy is hotter than its surroundings, thus temperatures decrease both upwards towards the atmosphere above the canopy and downwards towards the ground surface, resulting in an unstably stratified atmosphere above the canopy and a stably stratification region inside the canopy. Figure 1 shows the original time series of temperature $T$ and vertical wind velocity $w$ above and within the Amazon forest canopy.

![Fig. 1. Time series of temperature $T$ and vertical wind velocity $w$ above the Amazon forest canopy (left panels) and within the Amazon canopy (right panels), taken from noon to 12:30 on Julian Day 068, 1999.](image-url)
Fig. 2. Scale dependence of the normalized temperature-difference $\Delta T$ and the normalized vertical wind velocity-difference $\Delta w$ above the Amazon forest canopy for three different time scales ($\tau = 0.15$ s, 3.3 s and 100 s).

Fig. 3. Scale dependence of the normalized temperature-difference $\Delta T$ and the normalized vertical wind velocity-difference $\Delta w$ within the Amazon forest canopy for three different time scales ($\tau = 0.15$ s, 3.3 s and 100 s).

3 Intermittency and phase coherence in atmospheric turbulence

Figures 2 and 3 show, respectively, the scale dependence of the normalized temperature-difference $\Delta T = (\delta T - <\delta T>) / \sigma_T$ and the normalized vertical wind velocity-difference $\Delta w = (\delta w - <\delta w>) / \sigma_w$ above and within the Amazon forest canopy, respectively, for three different time scales ($\tau = 0.15$ s, 3.3 s and 100.0 s), where $\delta u = u(t + \tau) - u(t)$ denotes the two-point difference of vertical wind velocity $w$ or temperature $T$ for a given time scale $\tau$, the brackets denote the mean value of $\delta u$, and $\sigma_u$ denotes the standard deviation of $\delta u$. Evidently, the fluctuations in Figs. 2 and 3 become more intermittent as the scale becomes smaller.

The intermittent characteristics of Amazon atmospheric turbulence can be elucidated by the probability density function (PDF) of the temperature and vertical wind velocity fluctuations. Figure 4 shows the PDF of the normalized temperature-difference $\Delta T$ (right panels) and the normalized vertical wind velocity-difference $\Delta w$ (left panels) fluctuations above the Amazon forest canopy for 3 different scales ($\tau = 0.15$ s, 3.3 s and 100.0 s, indicated by a, b and c, respectively, in Fig. 7), superposed by a Gaussian PDF (gray line). Figure 5 shows the corresponding PDFs inside the Amazon forest canopy. It follows, from Figs. 4 and 5, that for both temperature and vertical wind velocity the PDF is close to the Gaussian distribution at large scale ($\tau = 100$ s) but deviates substantially from the Gaussian distribution as the scale $\tau$ decreases. At small scales ($\tau = 0.15$ s and 3.3 s) the shape of PDF becomes leptokurtic, exhibiting fat tails and sharp peaks. Figures 4 and 5 show that the tails of PDF get longer and the peaks of PDF get sharper as the scale decreases.

Intermittency can be quantified by calculating the variation of the normalized fourth-order structure function $K$ (kurtosis) with scale $\tau$, $K(\tau) = (1/n) \sum_{i=1}^{n} ((\delta u_i - <\delta u_i>) / \sigma_u)^4 - 3$. For an intermittent signal $K(\tau) > 0$ and $K$ increases when scale decreases; for a Gaussian noise $K = 0$ for all scales. Top panels of Figs. 6 and 7 show the computed variation of $K$ with scale $\tau$ for temperature and vertical wind velocity, above and inside the Amazon forest canopy, where the horizontal bar denotes the inertial subrange, approximately from 0.15 s to 3.3 s (Bolzan et al., 2002; Ramos et al., 2004), estimated by the method of Kulkarni et al. (1999) using isotropy coefficient calculated by the Haar wavelet transform.
An alternative way of quantifying intermittency is to apply the phase coherence technique using surrogate data by defining a phase coherence index (Hada et al., 2003; Koga et al., 2007, 2008), $C_\phi(\tau) = (S_{\text{PRS}}(\tau) - S_{\text{ORG}}(\tau)) / (S_{\text{PRS}}(\tau) - S_{\text{PCS}}(\tau))$. This index measures the degree of phase coherence in an original data set (ORG) by comparing it with two surrogate data sets created from the original data set: the phase-randomized surrogate (PRS) in which the phases of the Fourier modes are made completely random, and the phase-correlated surrogate (PCS) in which the phases of the Fourier modes are made completely equal. The power spectrum of three data sets ORG, PRS and PCS are kept the same, but their phase distributions are different. Each length of ORG, PRS and PCS data set is measured by the magnitude of first-order structure function $S_1(\tau) = \sum_{i=1}^{n} |u_{i+1} - u_i|$. An average of over 100 realizations of the phase shuffling is performed to generate the phase-randomized surrogate data set $S_{\text{PRS}}(\tau)$. $C_\phi(\tau) = 0$ indicates that the phases of the scales $\tau$ of the original data are completely random, whereas $C_\phi(\tau) = 1$ indicates that the phases are completely correlated. Bottom panels of Figs. 6 and 7 show the computed variation of $C_\phi$ with scale $\tau$ for temperature and vertical wind velocity above and inside the Amazon forest canopy.

Figure 6 confirms that both kurtosis and phase coherence index can be used to measure the degree of intermittency and phase coherence in turbulence. Left panels of Fig. 6 show that for all scales $\tau \lesssim 35$ s the in-canopy vertical velocity is more intermittent than the above-canopy vertical velocity. Right panels of Fig. 6 show that for small scales outside the inertial subrange the in-canopy temperature is more intermittent than the above-canopy temperature; whereas, for scales within and greater than the inertial subrange the in-canopy temperature is less intermittent than the above-canopy temperature.

4 Scalar-velocity dissimilarity in atmospheric intermittent turbulence

The dissimilarity between temperature (scalar) and vertical wind velocity (momentum) can be elucidated by Figs. 4, 5 and 7. Figure 4 shows that for scales $\tau = 0.15$ s and 3.3 s (a and b in Fig. 7) the PDFs of temperature fluctuations have longer tails and sharper peaks than the PDFs of vertical velocity fluctuations, implying that at these scales temperature is more intermittent than vertical wind velocity above the Amazon forest canopy. The scalar-velocity dissimilarity above the canopy is clearly characterized by both kurtosis and phase coherence techniques in the left panels of Fig. 7.
which show that the above-canopy temperature is more intermittent than vertical wind velocity for all scales $\tau \sim 55$ s.

In contrast, the right panels of Fig. 7 show that the scalar-velocity dissimilarity of the in-canopy turbulence is greatly reduced. The scalar-velocity similarity inside the canopy is evidenced in Fig. 5 which shows that, at $\tau = 0.15$ s the PDFs of temperature and vertical wind velocity have similar sharp peaks and long-tail statistics.

5 Conclusions

In this paper, we applied two different nonlinear techniques, kurtosis and phase coherence index, to analyze day-time atmospheric data above and within an Amazon forest canopy. We showed that the scale dependence of kurtosis and phase coherence index for vertical wind velocity and temperature above and within canopy exhibit similar behaviors, as seen in Fig. 6. In particular, both techniques demonstrate a clear enhancement of scalar-velocity similarity for in-canopy turbulence in comparison to its above-canopy counterpart, as seen in Fig. 7. Our results prove that the atmospheric intermittent turbulence, above and within the Amazon forest canopy, is generated by the phase coherence due to nonlinear wave-wave interactions. Turbulence consists of an admixture of chaos and noise. Recent studies have identified the chaotic nature of the solar-terrestrial environment (Macek, 1998; Chian et al., 2006) and the atmospheric turbulence above the Amazon forest (Campanharo et al., 2008), which have been confirmed by computer simulations of temporal chaos and spatiotemporal chaos in fluids and plasmas (Chian et al., 2006; Rempel and Chian, 2007; Rempel et al., 2007). It is likely that phase coherence and chaotic synchronization are the origin of energy bursts and coherent structures of turbulence in the complex earth-ocean-space system (He and Chian, 2003, 2005).

The turbulent exchange of mass and momentum from and within canopies is dominated by coherent structures (Finnigan, 2000). Wesson et al. (2003) applied three nonlinear time series techniques (Shannon entropy, wavelet thresholding, and mutual information content) to contrast the level of organization in vertical wind velocity in the canopy sublayer and the atmospheric surface layer. In the present paper, we have demonstrated that both kurtosis and phase coherence index techniques are capable of characterizing the degree of departure from Gaussianity, due to phase coherence, of atmospheric intermittent turbulence. The nonlinear techniques discussed in this paper can be applied to investigate the role played by coherent structures in experimental (Gao et al., 1989; Barthlott et al., 2007), theoretical (Raupach, 1996; Harman and Finnigan, 2007), and large-eddy simulation (Su et al., 1998; Qiu et al., 2008) studies of atmospheric turbulence in forest canopy, as well as in orchard canopy (Wang et al., 1992; Stoughton et al., 2002), rice canopy (Gao et al., 2003), corn canopy (Yue et al., 2007; Zhu et al., 2007), cotton and grape canopies (Mitic et al., 1999), coral canopy (Reidenbach et al., 2007), and urban canopy (Feigenwinter and Vogt, 2005; Salmond et al., 2005).
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