Event-Triggered $L_2 - L_\infty$ Filtering for Network-Based Neutral Systems With Time-Varying Delays via T-S Fuzzy Approach

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**ABSTRACT** This article examines the issue of event-triggered $L_2 - L_\infty$ filtering for network-based neutral systems via Takagi-Sugeno (T-S) fuzzy approach. A dynamic discrete event-triggered scheme (ETS) is introduced to save the limited communication resource. Based on the T-S fuzzy model, the considered neutral type system with networked induced delays are represented as a class of T-S fuzzy system. In addition, by considering a suitable Lyapunov-Krasovskii functional (LKF) and by using the Wirtinger inequality technique, the stability conditions with respect to linear matrix inequalities (LMIs) are presented to guarantee the considered filtering systems are asymptotically stable with $L_2 - L_\infty$ performance index $\gamma$. To the end, numerical examples are given to illustrate the effectiveness of the proposed result.

**INDEX TERMS** Event-triggered scheme, $L_2 - L_\infty$ filter, networked control systems, T-S fuzzy systems.

**I. INTRODUCTION**
Takagi-Sugeno (T-S) fuzzy model [1] has been widely used design and analysis of fuzzy control systems. Combining a set of IF-THEN rules with some fuzzy sets, makes it possible to approximate nonlinear systems with high precision using a series of linear subsystems. As a result, recent years have seen an increase in research interest in the control issues associated with T-S fuzzy systems [2]–[6]. The authors in [5] have discussed the stability of a T-S fuzzy system with state quantization under exponential dissipation using a non-fragile sampled-data control. For estimation of state variables in a digital sampled system, network-based estimation/ filtering is required. The standard Kalman filtering does not provide adequate results when the Gaussian noises with known statistics are not satisfied in real-world scenarios [7]–[10]. Thus, network-based filtering has gained much importance [11]–[15]. However, the nonlinear system filter design issue remains unsolvable due to the difficulty of analyzing nonlinear system stability. For this reason, over the last two decades, an increasing number of academics have dedicated themselves to move on to filtering. In addition, as a special case of time delay, the neutral delay occurs in the derivative of the state, not in the state itself. Recently, many researchers have focused on the neutral type delay with different controller techniques in [16], [17]. In [16], the authors discussed the $H_\infty$ filtering technique for T-S fuzzy neutral-type stochastic system.

Generally, the majority of the control tasks are executed periodically in numerous digital control applications. Considering the limited network resources, event-triggered control scheme (ETCS) has emerged as a successful technique to address this issue, which helps to reduce the amount of information that had to be transmitted, which helps to reduce...
network bandwidth occupation compared to a conventional periodic sampling technique. Lately, event-triggered filtering has gained more popularity, and key findings have been published [30]–[34]. The authors in [31] has been discussed the event-triggered fault detection filter method for nonlinear networked systems. Event-triggered filtering for nonlinear networked control systems with T-S fuzzy approach has been examined in [34].

On the other hand, the estimation of the system states and filtering is a popular issue in signal processing and control applications. Over the previous decade, the issue of filtering for the networked system has become a focal point of consideration, and numerous powerful methodologies have been created; see, for example, $H_\infty$, $L_2 - L_\infty$, and passive filtering. Among them, $H_\infty$ and $L_2 - L_\infty$ filtering are good options for disturbances with unknown characteristics [35]–[39]. Based on the above filtering methods, the $L_2 - L_\infty$ filtering can ensure that the error system is asymptotically stable and possesses a predefined $L_2 - L_\infty$ disturbance attenuation performance in the case when the disturbance is energy bounded. $L_2 - L_\infty$ filtering is aiming to make the estimation error’s peak value minimal for all distractions satisfying energy bound ability. Therefore, $L_2 - L_\infty$ filtering is preferred on the condition that the filtering error’s peak value is expected to be considered minimal. The filtering design techniques were introduced for different T–S fuzzy models in the literature’s [31], [34], [40]. To the author’s knowledge, the event-triggered $L_2 - L_\infty$ filtering for network-based neutral systems with time-varying delays via T-S fuzzy has not been fully investigated.

As a result of the preceding discussions, this article discusses event-triggered $L_2 - L_\infty$ filtering for network-based neutral T-S fuzzy systems. Furthermore, based on the suitable Lyapunov-Krasovskii functional (LKF), the delay stability conditions are derived from linear matrix inequalities (LMIs).

This article mainly focuses on the following points:

i). A new model of fuzzy filtering error system is provided under the consideration of dynamic discrete ETCS, which can save network resources.

ii). A novel dynamic discrete ETCS with different triggered thresholds is proposed for different fuzzy rules in terms of the considered error system. Compared with the existing work [19], [41], the proposed one in this paper, which can more effectively save the limited communication resources on the network while achieving good performance.

iii). The logical Zero Order Holder (ZOH) is used to actively discard packet failures and select the latest packet to drive the filter.

iv). By choosing the appropriate LKF, Wirtinger integral inequality approach, and the sufficient conditions ensure that the desired filtering system is asymptotically stable with respect to $L_2 - L_\infty$ performance; as a result, which plays a vital role in achieving less conservative results than [19], which can be evaluated in terms of LMIs.

v). Finally, various numerical examples are given to show the feasibility of the results with a practical application of the proposed method to a tunnel diode circuit model. This implies the merit of derived delay-dependent conditions.

Notation: For a matrix $Q$, $Q^{-1}$ noted as inverse and $Q^T$ means the transpose of $Q$, $R^n$ and $R^{n \times m}$ indicates the $n$-dimensional Euclidean space and set of $n \times m$ real matrix, respectively. For $\mathbb{Z}$ is a positive (negative) definite matrix, such that $\mathbb{Z} > 0$ ($\mathbb{Z} < 0$), and $I_n$ represents the identity matrix of dimension $n$, $*$ is used to represent the term that is induced by symmetry. $\mathbb{N}$ represents the set of positive integers. Maximum allowable upper bound (MAUB).

II. SYSTEM DESCRIPTION

Consider the following T-S fuzzy neutral system with disturbance:

Rule i: IF $s_1(t)$ is $F_{1i}$ and $s_2(t)$ is $F_{2i}$, ..., and $s_n(t)$ is $F_{ni}$, THEN

$$\begin{align*}
\dot{x}(t) &= A_0\hat{x}(t) + A_1\hat{x}(t - d(t)) \\
&\quad + A_2\hat{x}(t - h(t)) + B_1w(t), \\
\dot{y}(t) &= C_0\hat{x}(t), \\
z(t) &= E_0\hat{x}(t)
\end{align*}$$

(1)

where $s_1(t), s_2(t), \ldots, s_n(t)$ are the premise variables that has been measurable, and each $F_{ij}$ ($i = 1, 2, \ldots, q, j = 1, 2, \ldots, n$) is a fuzzy set. $i = 1, 2, \ldots, q, q$ noted as the number of IF-THEN rules. $\hat{x}(t) \in \mathbb{R}^n$ and $\dot{y}(t) \in \mathbb{R}^m$ noted as state variables and measured output of the system. $y(t) \in \mathbb{R}^p$ represents the signal to be estimated. $w(t) \in \mathbb{R}^m$ means the disturbance which refers to $L_2[0, \infty)$. $A_0, A_1, A_2, B_1, C_0$ and $E_0$ are known matrices with adjustable dimensions. Also $d(t)$ and $h(t)$ are time-varying delays, which satisfies $d_1 \leq d(t) \leq d_2$, $d(t) \leq \mu_1$ and $h_1 \leq h(t) \leq h_2$, $h(t) \leq \mu_2, h_1 = h_2 - h_1$.

Utilizing center-average defuzzifier, product interference and singleton fuzzifier the dynamic fuzzy model (1) can be represented as follows

$$\begin{align*}
\dot{x}(t) &= \sum_{i=1}^{q} u_i(s(t)) \left[ A_{0i}\hat{x}(t) + A_{1i}\hat{x}(t - d(t)) \\
&\quad + A_{2i}\hat{x}(t - h(t)) + B_{1i}w(t) \right], \\
\dot{y}(t) &= \sum_{i=1}^{q} u_i(s(t)) \left[ C_{0i}\hat{x}(t) \right], \\
z(t) &= \sum_{i=1}^{q} u_i(s(t)) \left[ E_{0i}\hat{x}(t) \right],
\end{align*}$$

(2)

with

$$u_i(s(t)) = \frac{\beta_i(s(t))}{\sum_{j=1}^{q} \beta_j(s(t))}, \quad \beta_i(s(t)) = \prod_{j=1}^{n} F_{ij}(s_j(t)),$$

(3)

in which $F_{ij}(s_j(t))$ is the grade of membership of $s_j(t)$ in $F_{ij}$. It is assumed that $\beta_i(s(t)) \geq 0$, $i = 1, \ldots, q$, $\sum_{i=1}^{q} \beta_i(s(t)) > 0$ for all $t$. Therefore, $u_i(s(t)) \geq 0$ and $\sum_{i=1}^{q} u_i(s(t)) = 1$ for all $t$. 

transmission delay and properties of ZOH, we have

\[ \hat{y}(t) = \sum_{i=1}^{q} u_i(s(t)) \left[ A_{fi} \hat{y}_i(t) + B_{fi} \hat{y}_i(t) \right], \]

\[ z_f(t) = \sum_{i=1}^{q} u_i(s(t)) \left[ C_{fi} \hat{y}_i(t) \right], \quad (7) \]

where \( A_{fi}, B_{fi} \) and \( C_{fi} \) are filter parameters to be determined. Substituting (6) into (7) yields

\[ \hat{x}_f(t) = \sum_{i=1}^{q} u_i(s(t)) \left[ A_{fi} \hat{x}_i(t) + B_{fi} \hat{y}_i(t) \right], \]

\[ z_f(t) = \sum_{i=1}^{q} u_i(s(t)) \left[ C_{fi} \hat{x}_i(t) \right]. \quad (8) \]

**C. TIME-DELAY MODELING OF THE FILTERING ERROR SYSTEM**

By the preceding discussion, the filtering error system can be modeled using an interval time delay.

Let \( \xi(t) = [\hat{x}(t), x_f(t)]^T \) and \( e(t) = z(t) - z_f(t) \). Then, the resulting error system can be expressed as follows:

\[ \dot{\xi}(t) = \sum_{i=1}^{q} u_i(s(t)) \sum_{j=1}^{q} u_j(s(t)) \left[ \begin{bmatrix} A_{fi} & 0 \\ 0 & A_{fi} \end{bmatrix} \right] \xi(t) + \begin{bmatrix} A_{fi} \\ 0 \end{bmatrix} \hat{x}(t-d(t)) + \begin{bmatrix} A_{fi} \\ 0 \end{bmatrix} \hat{x}(t-h(t)) + \begin{bmatrix} B_{fi} \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ B_{fi} \end{bmatrix} \xi(t) \]

\[ e(t) = \sum_{i=1}^{q} u_i(s(t)) \sum_{j=1}^{q} u_j(s(t)) \left[ \begin{bmatrix} E_{fi} - C_{fi} \end{bmatrix} \right] \xi(t). \quad (9) \]

The filtering error system (9) is subject to constraints

\[ \begin{bmatrix} \hat{y}(t+h) - \hat{y}(t+k) \end{bmatrix}^T \phi(\hat{y}(t+k)) \leq \delta \hat{y}^T(t+h) \phi(\hat{y}(t+k)), \quad (10) \]

where \( l = 1, 2, \ldots, k+1-k-1 \).

With reference to [40] and [42], the following two conditions hold: (i) If \( t_k h + h + \overline{\nu} \geq t_{k+1} h + u_{k+1} \), and function \( \nu(t) \) defined as

\[ \nu(t) = t - t_k h, t \in [t_k h + u_k, t_{k+1} h + u_{k+1}). \quad (11) \]

Obviously,

\[ u_k \leq \nu(t) \leq (t_{k+1} - t_k) h + u_{k+1} \leq h + \overline{\nu}, \quad (12) \]

(ii) \( t_k h + h + \overline{\nu} < t_{k+1} h + u_{k+1} \), considering the following two intervals

\[ [t_k h + u_k, t_{k+1} h + h + \overline{\nu}] \]

and \( [t_k h + h + \overline{\nu}, t_{k+1} h + h + \overline{\nu} + h] \).

Since \( u_k \leq \overline{\nu} \) and integer \( a \geq 1 \) we get

\[ t_k h + ah + \overline{\nu} < t_{k+1} h + u_{k+1} \leq t_k h + ah + h + \overline{\nu}. \]
Let
\[
\begin{align*}
T_0 &= \{t_k h + \nu_t, t_k h + \nu_t + h\} \\
T_i &= \{t_k h + i h + \nu_i, t_k h + i h + \nu_i + h\} \\
T_a &= \{t_k h + a h + \nu_i, t_k h + i h + a h + \nu_k+1\},
\end{align*}
\] 
(13)
where \( \ell = 1, 2, \cdots, a - 1 \). Then, we obtain
\[
[t_k h + \nu_t, t_k h + 1 h + \nu_k+1] = \bigcup_{i=0}^{a} T_i.
\] 
(14)
Define
\[
v(t) = \begin{cases} 
    t - t_k h, & t \in T_0 \\
    t - t_k h - i h, & t \in T_i \\
    t - t_k h - a h, & t \in T_a.
\end{cases}
\] 
(15)
Clearly, we have
\[
\begin{align*}
v_b &\leq v(t) < h + \nu, t \in T_0 \\
v_b &\leq \nu \leq v(t) < h + \nu, t \in T_i \\
v_b &\leq \nu \leq v(t) < h + \nu, t \in T_a.
\end{align*}
\] 
(16)
As a result,
\[
0 \leq v_b \leq v(t) < h + \nu, t \in [t_k h + \nu_t, t_k h + 1 h + \nu_k+1].
\] 
(17)
Furthermore, the following two cases are considered:
- Define \( e_k(t) = 0 \) for \( t \in [t_k h + \nu_t, t_k h + 1 h + \nu_k+1] \)
- Denote
\[
e_k(t) = \begin{cases} 
    0, & t \in T_0 \\
    \tilde{y}(t_k h) - \tilde{y}(t_k h + i h), & t \in T_i \\
    \tilde{y}(t_k h) - \tilde{y}(t_k h + a h), & t \in T_a.
\end{cases}
\] 
(18)
we obtain
\[
\tilde{y}(t_k h) = e_k(t) + \tilde{y}(t - \nu(t)).
\] 
(19)
Combining (9)-(19), the filtering error system can be written as
\[
\begin{align*}
\dot{\xi}(t) &= \sum_{i=1}^{q} \xi(s(t)) \sum_{j=1}^{q} u_j(s(t)) \left\{ \tilde{A}_0 \xi(t) + \tilde{A}_1 \tilde{y}(t - d(t)) \\
&+ \tilde{A}_2 \tilde{x}(t - h(t)) + \tilde{B} w(t) + \tilde{B}_1 e_k(t) + \tilde{C} \tilde{x}(t - \nu(t)) \right\}, \\
e(t) &= \sum_{i=1}^{q} \xi(s(t)) \sum_{j=1}^{q} u_j(s(t)) \tilde{E} \xi(t),
\end{align*}
\] 
where
\[
\tilde{A}_0 = \begin{bmatrix} A_{0i} & 0 \\ 0 & A_{fi} \end{bmatrix}, \quad \tilde{A}_1 = \begin{bmatrix} A_{1i} & 0 \\ 0 & 0 \end{bmatrix}, \\
\tilde{A}_2 = \begin{bmatrix} A_{2i} & 0 \\ 0 & 0 \end{bmatrix}, \quad \tilde{B} = \begin{bmatrix} B_i \\ 0 \end{bmatrix}, \quad \tilde{B}_1 = \begin{bmatrix} 0 \\ B_{fi} \end{bmatrix}, \\
\tilde{C} = \begin{bmatrix} 0 \\ B_{fi} C_i \end{bmatrix}, \quad \tilde{E} = \begin{bmatrix} E_i - C_{fi} \end{bmatrix}.
\]
For our convenience, the above filtering error system can be written as follows:
\[
\begin{align*}
\dot{\xi}(t) &= \tilde{A}_0 \xi(t) + \tilde{A}_1 \tilde{y}(t - d(t)) + \tilde{A}_2 \tilde{x}(t - h(t)) + \tilde{B} w(t) \\
&+ \tilde{B}_1 e_k(t) + \tilde{C} \tilde{x}(t - \nu(t)), \\
e(t) &= \tilde{E} \xi(t).
\end{align*}
\] 
(20)
where
\[
\begin{align*}
\tilde{A}_0 &= \begin{bmatrix} A_0 & 0 \\ 0 & A_f \end{bmatrix}, \quad \tilde{A}_1 &= \begin{bmatrix} A_1 & 0 \\ 0 & 0 \end{bmatrix}, \\
\tilde{A}_2 &= \begin{bmatrix} A_2 & 0 \\ 0 & 0 \end{bmatrix}, \quad \tilde{B} = \begin{bmatrix} B_i \\ 0 \end{bmatrix}, \quad \tilde{B}_1 = \begin{bmatrix} 0 \\ B_{fi} \end{bmatrix}, \\
\tilde{C} &= \begin{bmatrix} 0 \\ B_{fi} C_i \end{bmatrix}, \quad \tilde{E} = \begin{bmatrix} E_i - C_{fi} \end{bmatrix}.
\end{align*}
\]
Before proceeding, we introduce the following definition and lemmas, which will help to obtain our key results.

**Definition 1** [40]: For a given scalar \( \gamma > 0 \), the filtering error system (20) is asymptotically stable in terms of \( L_2 - L_\infty \) performance \( \gamma \) and \( w(t) \in L_2[0, \infty) \), if for initial condition, the following inequality holds:
\[
\|e(t)\|_\infty \leq \gamma \|w(t)\|_2
\] 
(21)
where
\[
\|e(t)\|_\infty = \sqrt{\sup_i \{e(t) e(t)\}} \\
\|w(t)\|_2 = \sqrt{\int_0^\infty w(t)^2 w(t) dt}.
\]

**Lemma 1** [43]: Given a matrix \( M_1 > 0 \), the subsequent inequality satisfies for every continuously differentiable function \( \varphi \) in \([b, c] \to \mathbb{R}^n\)
\[
(c - b) \int_b^c \varphi^T(s) M_1 \varphi(s) ds \geq \left( \int_b^c \varphi(s) ds \right)^T M_1 \left( \int_b^c \varphi(s) ds \right) + 3 \Theta M_1 \Theta,
\]
where \( \Theta = \int_b^c \varphi(s) ds - \frac{2}{c - b} \int_b^c \int_b^c \varphi(u) duds \).

**Lemma 2** [43]: For a given matrix \( P \), and vector function \( \xi : [b_1, b_2] \to \mathbb{R}^n \), the subsequent condition holds:
\[
\int_{b_1}^{b_2} \xi(T(s)) P \xi(s) ds \geq \frac{1}{b_2 - b_1} \Xi \begin{bmatrix} P & 0 \\ 0 & 3P \end{bmatrix} \Xi,
\]
where
\[
\Xi = \begin{bmatrix} \xi(b_2) - \xi(b_1) \\ \xi(b_2) + \xi(b_1) - \frac{2}{b_2 - b_1} \int_{b_1}^{b_2} \xi(s) ds \end{bmatrix}.
\]

**III. MAIN RESULTS**

**A. \( L_2 - L_\infty \) FILTERING PERFORMANCE ANALYSIS FOR THE NEUTRAL SYSTEM**

This section presents new delay-dependent conditions for the \( L_2 - L_\infty \) filtering performance analysis based on Definition 1, which ensure that the neutral system (20) is asymptotically
stable for a defined $L_2 - L_\infty$ performance $\gamma$. For clarity, we represent the matrix as follows:

$$
A_0 = \sum_{i=1}^{q} u_i(s(t))A_{0i}, \quad A_1 = \sum_{i=1}^{q} u_i(s(t))A_{1i},
$$
$$
A_2 = \sum_{i=1}^{q} u_i(s(t))A_{2i}, \quad B = \sum_{i=1}^{q} u_i(s(t))B_i,
$$
$$
C = \sum_{i=1}^{q} u_i(s(t))C_i, \quad E = \sum_{i=1}^{q} u_i(s(t))E_i,
$$
$$
A_f = \sum_{j=1}^{q} u_j(s(t))A_{fj}, \quad B_f = \sum_{j=1}^{q} u_j(s(t))B_{fj},
$$
$$
C_f = \sum_{j=1}^{q} u_j(s(t))C_{fj}.
$$

**Theorem 1:** For given positive scalars $d_1, d_2, h_1, h_2, \mu_1, \gamma > 0, \delta$, and $\mu_2$, the filtering error system (20) can reach asymptotically stable under the $L_2 - L_\infty$ performance index $\gamma$ and event-triggered control (10) if there exist matrices $Q = \begin{bmatrix} Q & E^T \\ \ast & \gamma^2 I \end{bmatrix} > 0, (\Pi_{ij})_{24 \times 24},$

where $(\Pi_{ij})_{24 \times 24},$

$$
\Pi_{ij}^{(1,1)} = 2Q_{11} + R_1 + R_2 + R_3 + d_1 U_1 + d_2 U_2 + (d_2 - d_1) U_3 - \frac{4}{h_1} U_4 - \frac{4}{h_2} U_5 - \frac{4}{v^2} P_3 + P_1 + P_2 + 2F_1 A_0,
$$
$$
\Pi_{ij}^{(1,4)} = 2Q_{11} + 2F_1 A_1, \quad \Pi_{ij}^{(1,5)} = \frac{2}{h_1} U_4,
$$
$$
\Pi_{ij}^{(1,6)} = -\frac{2}{h_2} U_5, \quad \Pi_{ij}^{(1,7)} = 2Q_{11} - \frac{2}{v^2} P_3,
$$
$$
\Pi_{ij}^{(1,14)} = \frac{6}{h_1^2} U_4, \quad \Pi_{ij}^{(1,15)} = \frac{6}{h_2^2} U_5,
$$
$$
\Pi_{ij}^{(1,17)} = \frac{6}{v^2} P_3, \quad \Pi_{ij}^{(1,19)} = -2F_1 + (F_1 A_0)^T,
$$
$$
\Pi_{ij}^{(1,22)} = 2Q_{11} + 2F_1 A_2, \quad \Pi_{ij}^{(1,23)} = 2Q_{11},
$$
$$
\Pi_{ij}^{(1,24)} = 2Q_{11} + 2F_1 B, \quad \Pi_{ij}^{(2,2)} = -R_1, \quad \Pi_{ij}^{(3,3)} = -R_2,
$$
$$
\Pi_{ij}^{(4,4)} = -(1 - \mu_1) R_3, \quad \Pi_{ij}^{(4,19)} = (F_1 A_1)^T,
$$
$$
\Pi_{ij}^{(5,5)} = \frac{4}{h_1} U_4 - 4(h_1)^2 U_6, \quad \Pi_{ij}^{(5,6)} = -2(h_1)^2 U_6,
$$
$$
\Pi_{ij}^{(5,14)} = \frac{6}{h_1^2} U_4, \quad \Pi_{ij}^{(5,16)} = 6(h_1) U_6,
$$
$$
\Pi_{ij}^{(6,6)} = \frac{4}{h_2} U_5 - 4(h_2)^2 U_6, \quad \Pi_{ij}^{(6,15)} = \frac{6}{h_2^2} U_5,
$$
$$
\Pi_{ij}^{(6,16)} = 6(h_1 U_6),
$$
$$
\Pi_{ij}^{(7,7)} = -P_1 - \frac{4}{v^2} P_3 + \delta CT^T C,
$$
$$
\Pi_{ij}^{(7,17)} = \frac{6}{v^2} P_3, \quad \Pi_{ij}^{(7,23)} = \delta CT^T \phi, \quad \Pi_{ij}^{(8,8)} = -\frac{4}{d_1} U_1,
$$
$$
\Pi_{ij}^{(8,9)} = \frac{6}{d_1^2} U_1, \quad \Pi_{ij}^{(9,9)} = -\frac{12}{d_1^2} U_1, \quad \Pi_{ij}^{(10,10)} = -\frac{4}{d_2} U_2,
$$
$$
\Pi_{ij}^{(10,11)} = \frac{6}{d_2^2} U_2, \quad \Pi_{ij}^{(11,11)} = -\frac{12}{d_2^2} U_2,
$$
$$
\Pi_{ij}^{(12,12)} = -\frac{4}{(d_2 - d_1)^2} U_3, \quad \Pi_{ij}^{(12,13)} = \frac{6}{(d_2 - d_1)^2} U_3,
$$
$$
\Pi_{ij}^{(13,13)} = \frac{12}{d_2 - d_1)^2} U_3, \quad \Pi_{ij}^{(14,14)} = \frac{12}{h_1^2} U_4,
$$
$$
\Pi_{ij}^{(15,15)} = \frac{12}{h_2^2} U_5, \quad \Pi_{ij}^{(16,16)} = -12U_6,
$$
$$
\Pi_{ij}^{(17,17)} = \frac{4}{v^2} P_2 - \frac{12}{v^2} P_3, \quad \Pi_{ij}^{(17,18)} = 12U_2,
$$
$$
\Pi_{ij}^{(18,18)} = -\frac{12}{v^2} P_2, \quad \Pi_{ij}^{(19,19)} = R_4 + R_5 + R_6 + h_1 U_4 + h_2 U_5 + (h_1)^2 U_6 + \nu P_3 - 2F_1,
$$
$$
\Pi_{ij}^{(19,22)} = 2F_1 A_2, \quad \Pi_{ij}^{(19,24)} = 2F_1 B,
$$
$$
\Pi_{ij}^{(20,20)} = -R_4, \quad \Pi_{ij}^{(21,21)} = -R_5,
$$
$$
\Pi_{ij}^{(22,22)} = -(1 - \mu_2) R_6, \quad \Pi_{ij}^{(23,23)} = -(1 - \delta) \phi,
$$
$$
\Pi_{ij}^{(24,24)} = -I.
$$

**Proof:** Construct a Lyapunov–Krasovskii functional (LKF) candidate as,

$$
V(t) = \sum_{i=1}^{6} V_i(t),
$$

where

$$
V_1(t) = \xi^T(t) Q \xi(t),
$$
$$
V_2(t) = \int_{t-d_1}^{t} \dot{\xi}(s) R_1 \dot{\xi}(s) ds + \int_{t-d_2}^{t} \dot{\xi}(s) R_2 \dot{\xi}(s) ds,
$$
$$
+ \int_{t-d_1}^{t} \dot{\xi}(s) R_3 \dot{\xi}(s) ds,
$$
$$
V_3(t) = \int_{t-h_1}^{t} \dot{\xi}(s) R_4 \dot{\xi}(s) ds + \int_{t-h_2}^{t} \dot{\xi}(s) R_5 \dot{\xi}(s) ds,
$$
$$
+ \int_{t-h_1}^{t} \dot{\xi}(s) R_6 \dot{\xi}(s) ds,
$$
$$
V_4(t) = \int_{t-d_1}^{t} \int_{t+\theta}^{t} \dot{\xi}(s) U_1 \dot{\xi}(s) ds d\theta + \int_{t-d_2}^{t} \int_{t+\theta}^{t} \dot{\xi}(s) U_5 \dot{\xi}(s) ds d\theta,
$$
$$
V_5(t) = \int_{t-h_1}^{t} \int_{t+\theta}^{t} \dot{\xi}(s) U_4 \dot{\xi}(s) ds d\theta + \int_{t-h_2}^{t} \int_{t+\theta}^{t} \dot{\xi}(s) U_5 \dot{\xi}(s) ds d\theta,
$$
\[ V_6(t) = \int_{t-v}^{t} \hat{x}(s)P_1\hat{x}(s)ds + \int_{0}^{t} \hat{x}(s)P_2\hat{x}(s)ds \]

Taking the time derivative as follows:

\[ \dot{V}_1(t) = 2\tilde{\xi}(t)Q\tilde{x}(t), \]
\[ \dot{V}_2(t) \leq \dot{x}^T(t)(R_1 + R_2 + R_3)\tilde{x}(t) - \dot{x}^T(t)(d(t) - d_1) - \dot{x}^T(t)(d_2)R_3\tilde{x}(t) - (1 - \mu_1)\tilde{x}(t)(d(t) - d(t)), \]
\[ \dot{V}_3(t) \leq \dot{x}^T(t)(R_4 + R_5 + R_6)\tilde{x}(t) - \dot{x}^T(t)(h(t) - h) - \dot{x}^T(t)(h_2)R_5\tilde{x}(t) - (1 - \mu_2)\tilde{x}(t)(h(t) - h), \]
\[ \dot{V}_4(t) = \dot{x}^T(t)(d_1U_1 + d_2U_2 + (d_2 - d_1)U_3)\tilde{x}(t) - \int_{t-d_1}^{t} \dot{x}(s)U_1\hat{x}(s)ds - \int_{t-d_2}^{t} \dot{x}(s)U_2\hat{x}(s)ds - \int_{t-d_2}^{t} \dot{x}(s)U_3\hat{x}(s)ds. \]

By Lemma 1, then

\[ -\int_{t-d_1}^{t} \dot{x}^T(s)U_1\hat{x}(s)ds \leq -\frac{1}{d_1}(\int_{t-d_1}^{t} \hat{x}(s)ds)^T \hat{x}(s)ds \]
\[ \leq -\frac{1}{d_1}(\int_{t-d_1}^{t} \hat{x}(s)ds)^T \hat{x}(s)ds \]
\[ \leq -\frac{1}{d_1}(\int_{t-d_1}^{t} \hat{x}(s)ds)^T \hat{x}(s)ds \]
\[ \leq -\frac{1}{d_1}(\int_{t-d_1}^{t} \hat{x}(s)ds)^T \hat{x}(s)ds \]

Using Lemma 1 and 2, then

\[ -\int_{t-v}^{t} \dot{x}^T(s)P_2\hat{x}(s)ds \leq -\frac{1}{v}(\int_{t-v}^{t} \hat{x}(s)ds)^T \hat{x}(s)ds \]

Similarly,

\[ -\int_{t-v}^{t} \dot{x}^T(s)P_3\hat{x}(s)ds \leq -\frac{1}{v}(\int_{t-v}^{t} \hat{x}(s)ds)^T \hat{x}(s)ds \]

Furthermore, the following condition is satisfied for any properly dimensioned matrix \( F_1 \):

\[ 2[\dot{x}^T(t)F_1 + \dot{x}^T(t)F_1][\hat{x}(t) + A_0\hat{x}(t)] + A_1\hat{x}(t - d(t)) + A_2\hat{x}(t - h(t)) + Bw(t) = 0. \]
Based on ETCS (10) and $w(t) = 0$, we obtain

$$e_k^T(t)e_k(t) \leq \delta(e_k(t) + C\hat{x}(t - \nu(t)))^T \phi e_k(t) + C\hat{x}(t - \nu(t))),$$

which corresponds to

$$\begin{bmatrix} \hat{x}(t - \nu(t)) \end{bmatrix}^T \begin{bmatrix} \delta C^T \phi \delta C^T \phi \end{bmatrix} \begin{bmatrix} (\delta - 1)\phi \end{bmatrix} \times \begin{bmatrix} \hat{x}(t - \nu(t)) \end{bmatrix} \geq 0.$$ (41)

Combining (25)-(41) yields

$$\hat{V}(t) \leq \xi^T(t)\psi(t)\xi(t),$$ (42)

in which

$$\xi^T(t) = \left[\xi^T(t), \xi^T(t - d_1(t)), \xi^T(t - d_2(t)), \xi^T(t - h_1(t)), \xi^T(t - h_2(t))\right],$$

and ($\psi(t)$) are defined as follows:

$$\psi(t)_{11} = \frac{2Q\bar{A}_0 + R_1 + R_2 + R_3 + d_1U_1 + d_2U_2}{h_1U_4},$$

$$\psi(t)_{12} = \frac{4}{h_2U_5} - \frac{4}{h_2U_4} - \frac{4}{h_2U_5} - \frac{4}{h_2P_3},$$

$$\psi(t)_{13} = \frac{P_1 + \nu P_2 + 2F_1A_0}{h_1U_4},$$

$$\psi(t)_{14} = \frac{2Q\bar{A}_1 + 2F_1A_1}{h_1U_4},$$

$$\psi(t)_{15} = \frac{-2}{h_2U_5},$$

$$\psi(t)_{16} = \frac{2Q\sigma - \frac{2}{V}P_3}{h_2U_5},$$

$$\psi(t)_{17} = \frac{6}{h_2}U_4,$$ (43)

$$\psi(t)_{18} = \frac{6}{h_2U_5},$$ (44)

In view of the condition (42) $\psi(t) < 0$, indicates that $\hat{V}(t) < 0$, with the end that the filtering error system (20) for ETCS (10) with $w(t) = 0$ is asymptotically stable.

In addition, when $w(t) \neq 0$, we calculate the $L_2 - L_\infty$ performance of the filtering error system (20) as follows: Consider the index

$$J = V(t) - \int_0^t w^T(s)w(s)ds.$$ (45)

For all nonzero $w(t) \in L_2[0, +\infty)$, we get

$$J = \int_0^t (\hat{V}(s) - w^T(s)w(s))ds \leq \xi^T(t)[\psi(t)]\xi(t).$$ (46)

Where $\xi(t) = [\xi^T(t), w^T(t)].$ Applying the Schur complement to (44), we know that (22) guarantees $J < 0$, implying

$$\xi^T(t)Q\xi(t) \leq V(t) < \int_0^t w^T(s)w(s)ds.$$ (47)

Meanwhile, using Schur complement to (23), we know that $E^T\tilde{E} < \gamma^2 Q$. Then, it is simple to see that for every $t \geq 0$

$$e^T(t)\xi(t) = e^T(t)E^T\tilde{E}\xi(t) < \gamma^2 \xi^T(t)Q\xi(t) < \gamma^2 \int_0^t w^T(s)w(s)ds < \gamma^2 \int_0^\infty w^T(s)w(s)ds.$$ (48)

Therefore, by Definition 1, the filtering error system (20) is asymptotically stable with an $L_2 - L_\infty$ performance $\gamma$. 
B. \(L_2 - L_{\infty}\) FILTER DESIGN FOR THE NEUTRAL SYSTEM

In reference to the \(L_2 - L_{\infty}\) performance analysis in Theorem 1, in this part, we will provide a sufficient condition to derive the existence of event-triggered \(L_2 - L_{\infty}\) filter of the form (8) in the subsequent Theorem 2.

Theorem 2: For given positive scalars \(d_1, d_2, h_1, h_2, \nu, \mu_1, \gamma > 0, \delta, \) and \(\mu_2,\) the \(L_2 - L_{\infty}\) filtering system (20) is solvable if there exist matrices \(S > 0, Q_1 > 0, R_1 > 0, U_1 > 0, P_m > 0, \phi > 0, l = 1, 2, 3, 4, 5, 6, m = 1, 2, 3\) and positive diagonal matrix \(F_1\) and \(\bar{A}_f, \bar{B}_f, \bar{C}_f\) with adjustable dimensions, such that the following LMIs hold:

\[
\begin{bmatrix}
Q_1 & S & E^T \\
* & S & -C^T_f \\
* & * & \gamma^2 I
\end{bmatrix} > 0,
\]

where

\[
\begin{align*}
\phi_{ij}^{(1,1)} &= R_1 + R_2 + R_3 + d_1 U_1 + d_2 U_2 + \delta t \frac{4}{h_2} U_4 - \frac{4}{h_2} U_4 - \frac{4}{h_1} U_4 + \frac{4}{h_2} U_4 - \frac{4}{\nu} P_3 + P_1 + \nu P_2 + 2 F_1 A_0 + 2 Q_1 A_0, \\
\phi_{ij}^{(1,2)} &= A_f^T S + \bar{A}_f, \phi_{ij}^{(1,5)} = 2 F_1 A_1 + Q_1 A_1, \\
\phi_{ij}^{(1,6)} &= -\frac{4}{h_1} U_4, \phi_{ij}^{(1,7)} = -\frac{4}{h_2} U_4, \\
\phi_{ij}^{(1,8)} &= -\frac{2}{h_1} P_3 + \bar{B}_f C, \phi_{ij}^{(1,15)} = -\frac{6}{h_2} U_4, \\
\phi_{ij}^{(1,16)} &= \frac{6}{h_2} U_5, \phi_{ij}^{(1,18)} = \frac{6}{h_2} U_5, \\
\phi_{ij}^{(1,20)} &= -2 F_1 + (F_1 A_0) + 2 Q_1 A_2, \\
\phi_{ij}^{(1,24)} &= \bar{B}_f, \phi_{ij}^{(1,25)} = 2 F_1 B + Q_1 B, \\
\phi_{ij}^{(2,2)} &= 2 \bar{A}_f, \phi_{ij}^{(2,25)} = \bar{A}_f^T A_1 + Q_1^2 B, \phi_{ij}^{(2,25)} = \bar{B}_f C, \\
\phi_{ij}^{(2,3)} &= \bar{A}_f^T A_1, \phi_{ij}^{(2,24)} = \bar{B}_f, \phi_{ij}^{(2,25)} = \bar{Q}_1 B, \\
\phi_{ij}^{(2,3)} &= -R_1, \phi_{ij}^{(4,4)} = -R_2, \phi_{ij}^{(5,5)} = -(1 - \mu_1) R_3, \\
\phi_{ij}^{(5,20)} &= (F_1 A_1)^T, \phi_{ij}^{(6,6)} = -\frac{4}{h_1} U_4 - 4(h_1)^2 U_4, \\
\phi_{ij}^{(6,7)} &= -2(h_1)^2 U_6, \phi_{ij}^{(6,15)} = \frac{6}{h_2} U_4, \\
\phi_{ij}^{(6,17)} &= 6(h_1)^2 U_6, \\
\phi_{ij}^{(7,7)} &= -\frac{4}{h_2} U_5 - (h_1)^2 U_5, \\
\phi_{ij}^{(7,16)} &= \frac{6}{h_2} U_5, \phi_{ij}^{(7,17)} = 6(h_1)^2 U_6, \\
\phi_{ij}^{(8,8)} &= -P_1 - \frac{4}{\nu} P_3 + \delta C^T \phi C, \\
\phi_{ij}^{(8,18)} &= \frac{6}{h_1} P_3, \phi_{ij}^{(8,24)} = \delta C^T \phi, \\
\phi_{ij}^{(9,9)} &= -\frac{4}{d_1} U_1, \phi_{ij}^{(9,10)} = \frac{6}{d_1} U_1, \\
\phi_{ij}^{(10,10)} &= \frac{12}{d_1^3} U_1, \phi_{ij}^{(11,11)} = \frac{4}{d_2^2} U_2, \phi_{ij}^{(11,12)} = \frac{6}{d_2^2} U_2.
\end{align*}
\]

Moreover the desired filter of the form (7) is given by

\[
A_f = S^{-1} \bar{A}_f, B_f = S^{-1} \bar{B}_f, C_f = \bar{C}_f.
\]

Proof: Since \(S > 0,\) there exists a real matrix \(Q_2\) and \(Q_3 > 0,\) such that \(S = Q_2 Q_3^T Q_2^T\). Defining \(H = \text{diag}(I, Q_2 Q_3^{-1}, \bar{A}_f, \bar{B}_f, \bar{C}_f)\) and denoting \(\bar{A}_f = Q_2 A_f Q_3^{-1} Q_2^T, \bar{B}_f = Q_2 B_f, \bar{C}_f = C_f.\) Multiplying by both sides on \(H\) and \(H^T\), then we get (47) and (48). According to Theorem 1, if (47) and (48) are feasible, the ETCS \(L_2 - L_{\infty}\) problem is solvable, the filtering parameters are described by (49).

Remark 1: Consider the following filtering system from (20) without neutral delay as follows:

\[
\dot{\xi}(t) = \bar{A}_f \dot{\xi}(t) + \bar{A}_1 \dot{x}(t - d) + \bar{B} w(t) + \bar{B}_1 e(t) + \bar{C} \dot{x}(t - \nu(t)),
\]

\[
e(t) = \bar{E} \xi(t),
\]

Using the similar methods in Theorem 2, we can get the following results.

Corollary 1: For given positive scalars \(d_1, d_2, \nu, \mu_1, \gamma > 0,\) \(\delta,\) the \(L_2 - L_{\infty}\) filtering system (50) is solvable if there exist positive definite matrices \(S > 0, Q_1 > 0, R_1 > 0, U_1 > 0, P_m > 0, \phi > 0, l = 1, 2, 3, m = 1, 2, 3\) and diagonal matrix \(F_1 > 0\) and \(\bar{A}_f, \bar{B}_f, \bar{C}_f\) with appropriate dimensions such that

\[
\begin{bmatrix}
Q_1 & S & E^T \\
* & S & -C^T_f \\
* & * & \gamma^2 I
\end{bmatrix} > 0,
\]

where

\[
\begin{align*}
\phi_{ij}^{(1,1)} &= R_1 + R_2 + R_3 + d_1 U_1 + d_2 U_2 + (d_2 - d_1) U_3, \\
\phi_{ij}^{(13,14)} &= -\frac{4}{d_2 - d_1} U_3, \\
\phi_{ij}^{(13,15)} &= -\frac{4}{d_2 - d_1} U_3, \\
\phi_{ij}^{(17,18)} &= -\frac{4}{d_2 - d_1} U_3, \\
\phi_{ij}^{(19,19)} &= -\frac{4}{d_2 - d_1} U_3, \\
\phi_{ij}^{(22,22)} &= -\frac{4}{d_2 - d_1} U_3, \\
\phi_{ij}^{(24,24)} &= -\frac{4}{d_2 - d_1} U_3.
\end{align*}
\]
\[
\zeta_{ij}^{(1,6)} = \frac{2}{v} P_3 + B_f C_f, \quad \zeta_{ij}^{(1,13)} = \frac{6}{v^2} P_3, \\
\zeta_{ij}^{(1,15)} = -2F_1 + (F_1 A_0)^T, \quad \zeta_{ij}^{(1,16)} = B_f, \\
\zeta_{ij}^{(1,17)} = 2F_1 B + Q_1 B, \quad \zeta_{ij}^{(2,2)} = 2A_f, \\
\zeta_{ij}^{(2,5)} = Q_1^T A_1, \quad \zeta_{ij}^{(2,6)} = B_f C_f, \quad \zeta_{ij}^{(2,16)} = B_f, \\
\zeta_{ij}^{(2,17)} = Q_1^T B_f, \quad \zeta_{ij}^{(3,3)} = -R_1, \quad \zeta_{ij}^{(4,4)} = -R_2, \\
\zeta_{ij}^{(5,5)} = -(1 - \mu_1) R_3, \quad \zeta_{ij}^{(5,15)} = (F_1 A_1)^T, \\
\zeta_{ij}^{(6,6)} = -P_1 - \frac{4}{v} P_3 + \delta C^T \phi C_f, \\
\zeta_{ij}^{(6,13)} = \frac{6}{v^2} P_3, \quad \zeta_{ij}^{(6,16)} = \delta C^T \phi, \quad \zeta_{ij}^{(7,7)} = -\frac{4}{d_1} U_1, \\
\zeta_{ij}^{(7,8)} = \frac{6}{d_1^2} U_1, \quad \zeta_{ij}^{(8,8)} = \frac{12}{d_1^2} U_1, \quad \zeta_{ij}^{(9,9)} = -\frac{4}{d_2} U_2, \\
\zeta_{ij}^{(9,10)} = \frac{6}{d_2^2} U_2, \quad \zeta_{ij}^{(10,10)} = -\frac{12}{d_2^2} U_2, \\
\zeta_{ij}^{(11,11)} = -\frac{4}{d_2 - d_1} U_3, \quad \zeta_{ij}^{(11,12)} = \frac{6}{(d_2 - d_1)^2} U_3, \\
\zeta_{ij}^{(12,12)} = -\frac{12}{d_2 - d_1} U_3, \quad \zeta_{ij}^{(13,13)} = -\frac{4}{v} P_2 - \frac{12}{v^3} P_3, \\
\zeta_{ij}^{(13,14)} = \frac{6}{v^2} P_2, \quad \zeta_{ij}^{(14,14)} = \frac{12}{v^3} P_2, \\
\zeta_{ij}^{(15,15)} = v P_3 - 2F_1, \quad \zeta_{ij}^{(15,17)} = 2F_1 B, \\
\zeta_{ij}^{(16,16)} = -(1 - \delta) \phi, \quad \zeta_{ij}^{(17,17)} = -I.
\]

Moreover the desired filter of the form (7) is given by
\[
A_f = S^{-1} A_f, \quad B_f = S^{-1} B_f, \quad C_f = C_f.
\]  
(53)

**Proof:** The proof is similar process in Theorem 2.

**Remark 2:** Consider the following linear system (similar as in [17]), which is given by
\[
\hat{x}(t) = A_0 \hat{x}(t) + A_1 \hat{x}(t - d(t)) + A_2 \hat{x}(t - h(t)).
\]  
(54)

According to Theorem 1, we can derive the following Corollary 2 for the asymptotic stability of the neutral type system (54).

**Corollary 2:** For given positive scalars \(d_1, d_2, h_1, h_2, \mu_1\) and \(\mu_2\), the system (54) is solvable if there exist matrices \(Q_1 > 0, R_1 > 0, U_i > 0, i = 1, 2, 3, 4, 5, 6\), and positive diagonal matrix \(F_1\), such that the following LMI holds:
\[
\Phi < 0,
\]  
(55)

where \(\Phi = (\Phi_{ij})_{19 \times 19}\)
\[
\Phi^{(1,1)} = R_1 + R_2 + R_3 + d_1 U_1 + d_2 U_2 + (d_2 - d_1) U_3 - \frac{4}{h_1} U_4 - \frac{4}{h_2} U_5 + 2F_1 A_0 + 2Q_1 A_0, \\
\Phi^{(1,4)} = 2F_1 A_1 + Q_1 A_1, \quad \Phi^{(1,5)} = -\frac{2}{h_1} U_4, \\
\Phi^{(1,6)} = -\frac{2}{h_2} U_5, \quad \Phi^{(1,13)} = \frac{6}{h_1^2} U_4, \quad \Phi^{(1,14)} = \frac{6}{h_2^2} U_5, \\
\Phi^{(1,16)} = -2F_1 + (F_1 A_0)^T, \quad \Phi^{(1,19)} = 2F_1 A_2 + Q_1 A_2, \\
\Phi^{(2,2)} = -R_1, \quad \Phi^{(3,3)} = -R_2, \quad \Phi^{(4,4)} = -(1 - \mu_1) R_3, \\
\Phi^{(4,16)} = (F_1 A_1)^T, \quad \Phi^{(5,5)} = -\frac{4}{h_1} U_4 - 4(h_1^2) U_6, \\
\Phi^{(5,6)} = -2(h_1^2) U_6, \quad \Phi^{(5,13)} = \frac{6}{h_1^2} U_4, \\
\Phi^{(5,15)} = 6(h_1^2) U_6, \quad \Phi^{(6,6)} = \frac{4}{h_2} U_5 - 4(h_2^2) U_6, \\
\Phi^{(6,14)} = \frac{6}{h_2^2} U_5, \quad \Phi^{(6,15)} = 6(h_2^2) U_6, \\
\Phi^{(7,7)} = -\frac{4}{d_1^2} U_1, \quad \Phi^{(7,8)} = \frac{6}{d_1^2} U_1, \\
\Phi^{(8,8)} = -\frac{12}{d_2^3} U_2, \quad \Phi^{(9,9)} = -\frac{4}{d_2} U_2, \quad \Phi^{(9,10)} = \frac{6}{d_2} U_2, \\
\Phi^{(10,10)} = -\frac{12}{d_2^3} U_3, \quad \Phi^{(12,12)} = -\frac{12}{(d_2 - d_1)^3} U_3, \\
\Phi^{(13,13)} = -\frac{12}{h_1^2} U_4, \quad \Phi^{(14,14)} = -\frac{12}{h_2^2} U_5, \quad \Phi^{(15,15)} = -12 U_6, \\
\Phi^{(16,16)} = R_4 + R_5 + R_6 + h_1 U_4 + h_2 U_5 + (h_1^2) U_6 - 2F_1, \quad \Phi^{(16,19)} = 2F_1 A_2, \\
\Phi^{(17,17)} = -R_4, \quad \Phi^{(18,18)} = -R_5, \quad \Phi^{(19,19)} = -(1 - \mu_2) R_6.
\]

**Proof:** Consider the following LKF candidate
\[
V(t) = \sum_{i=1}^{5} V_i(t),
\]

\[V_1(t) = \int_{t-d(t)}^{t} \hat{x}^T(s) R_1 \hat{x}(s) ds + \int_{t-d(t)}^{t} \hat{x}^T(s) R_2 \hat{x}(s) ds + \int_{t-d(t)}^{t} \hat{x}^T(s) R_3 \hat{x}(s) ds,
\]

\[V_2(t) = \int_{t-h(t)}^{t} \hat{x}^T(s) R_4 \hat{x}(s) ds + \int_{t-h(t)}^{t} \hat{x}^T(s) R_5 \hat{x}(s) ds + \int_{t-h(t)}^{t} \hat{x}^T(s) R_6 \hat{x}(s) ds,
\]

\[V_4(t) = \int_{t-h(t)}^{t} \hat{x}^T(s) U_1 \hat{x}(s) ds + \int_{t-h(t)}^{t} \hat{x}^T(s) U_2 \hat{x}(s) ds + \int_{t-h(t)}^{t} \hat{x}^T(s) U_3 \hat{x}(s) ds + \int_{t-h(t)}^{t} \hat{x}^T(s) U_4 \hat{x}(s) ds + \int_{t-h(t)}^{t} \hat{x}^T(s) U_5 \hat{x}(s) ds + \int_{t-h(t)}^{t} \hat{x}^T(s) U_6 \hat{x}(s) ds,
\]

(56)

Then, using the same treatment theory as Theorem 1, we can easily get the Corollary 2.

**Remark 3:** Notice that Theorem 2 gives an adequate condition to co-plan the event-triggered filtering (8) and the event-triggered scheme in the communication (4). If the LMI
Example 3 is given to benchmark the proposed filter design. By comparing the results in the previous literature, the advantage of the system (57) is feasible, and the desired filter parameters $A$, $B$, and $C$ can be obtained.

Remark 4: In addition, computational complexity becomes a major issue, based on the size of the LMIs and the number of decision variables. However, larger LMIs improve performance. In recent years, an increasing number of researchers are working to improve the performance of time-delayed systems. The basic problem with time-delayed systems is to build better LKFIs and estimate their derivatives using better integral inequality techniques. The proposed stability criteria in this study are derived from the constructions of various LKFs; the proposed LMI conditions are more complicated and have computational complexity. To meet these needs, some new research has been recently published using a different type of LKF that is more effective at reducing computational complexity while keeping less conservative results [44], [45]. In future work, we will apply Finsler’s Lemma to reduce the number of decision variables and use this type of new LKF to reduce maintainability along with simple LMI conditions. Therefore, it is easy to use the provided method to reduce the maintainability and computational load of time-delayed systems with the new LKF in [44], [45].

IV. NUMERICAL EXAMPLES

In this part, numerical simulation results and application examples are provided to illustrate the designed filter’s performance. Example 1 shows the feasibility of Theorem 2. By comparing the results in the previous literature, the advantages of the proposed result are presented in Example 2. Example 3 is given to benchmark the proposed filter design through studying a tunnel diode circuit.

Example 1: Consider the following TS fuzzy neutral type system (57)

$$
\begin{align*}
\dot{x}(t) &= \tilde{A}_0 \tilde{x}(t) + \tilde{A}_1 \tilde{x}(t - d(t)) + \tilde{A}_2 \tilde{x}(t - h(t)) \\
&\quad + Bw(t) + B_1 \xi_k(t) + C \hat{\xi}(t - \nu(t)), \\
e(t) &= \bar{E} \tilde{x}(t),
\end{align*}
$$

with the following parameters:

- $A_{01} = \begin{bmatrix} -2 & 0 \\ 0 & -1 \end{bmatrix}$, $A_{02} = \begin{bmatrix} -2 & 0 \\ 0 & -2 \end{bmatrix}$, $A_{11} = \begin{bmatrix} -1 & 0 \\ -0.5 & -0.9 \end{bmatrix}$, $A_{12} = \begin{bmatrix} -0.9 & 0 \\ -1 & -0.8 \end{bmatrix}$, $A_{21} = \begin{bmatrix} 0.3 & -0.15 \\ 0.5 & -0.2 \end{bmatrix}$, $A_{22} = \begin{bmatrix} 0.4 & -0.1 \\ 0.5 & -0.3 \end{bmatrix}$
- $B_1 = \begin{bmatrix} 2 \\ -0.5 \end{bmatrix}$, $B_2 = \begin{bmatrix} 0.8 \\ 0.3 \end{bmatrix}$, $C_1 = \begin{bmatrix} 2 & 1 \end{bmatrix}$, $C_2 = \begin{bmatrix} 0.2 & -1 \end{bmatrix}$, $E_1 = \begin{bmatrix} 2 \\ -0.5 \end{bmatrix}$, $E_2 = \begin{bmatrix} -0.5 & 0.2 \end{bmatrix}$

The membership functions are taken as $u_1(s(t)) = \begin{cases} \frac{3 + \xi(t)}{3} \leq \tilde{x}(t) \leq 0; \\
\frac{3 - \xi(t)}{3} \leq \tilde{x}(t) \leq 3; \\
0 & \text{otherwise,}
\end{cases}$

and $u_2(s(t)) = 1 - u_1(s(t))$.

Subsequently, we will show the desired performance of the proposed ETCS (4) and the full order filter (7) for the system (1) with $L_2 - L_\infty$ performance index $\gamma$ according to Theorem 2. Before computation analysis, we assume $0.1 \leq d(t) \leq 0.2$, $0.2 \leq h(t) \leq 0.4$, $\mu_1 = 0.2$, $\mu_2 = 0.3$, $\nu = 0.01$, the external disturbances $\sigma(t) = \sin(0.1t)e^{(-0.1t)}$ and by applying the LMIs in Theorem 2, we can obtain the related trigger matrix $\phi = 2.0324$, and the following desired filter parameters:

$A_{f1} = \begin{bmatrix} -15.0634 & -2.3412 \\ -4.1445 & -14.5469 \end{bmatrix}$, $B_{f1} = \begin{bmatrix} -0.5487 \\ -1.2421 \end{bmatrix}$,

$C_{f1} = [0.5314 \ 0.4478]$, $A_{f2} = \begin{bmatrix} -16.1543 & -3.5428 \\ -4.2432 & -15.3678 \end{bmatrix}$, $B_{f2} = \begin{bmatrix} -0.6742 \\ -0.4587 \end{bmatrix}$, $C_{f2} = [0.4812 \ 0.3733]$.

Consider the initial state $\hat{x}(0) = [0.2 \ -0.1]^T$ and $x_f(t) = [-1 \ 0.5]^T$. The related simulation results are displayed in Figure 2, Figure 2a present the state responses of $\hat{x}(t)$, the corresponding curves of the state $\hat{x}(t)$, $\hat{x}_2(t)$ and $x_f(t)$, $x_f(t)$ are drawn in Figure 2b and Figure 2c, evolution of the error responses $e(t) = z(t) - \hat{z}(t)$ are depicted in Figure 2d. Based on the above Figures 2a-2d, that the filtering error system is asymptotically stable in terms of $L_2 - L_\infty$ performance by applying the designed parameters. Furthermore, because of the event-triggered mechanism, the release instants and release intervals are shown in Figure 2e. Finally, figure 2f depicts the corresponding state responses of the considered neutral type fuzzy filtering system with different initial values. In view of the above simulation studies, the proposed event-triggered mechanism with modelled system (20) can significantly minimize the data communication burden. We can conclude that the event-triggered scheme-based filter designed here works well while minimizing unnecessary communication data.

**TABLE 1.** Minimum $L_2 - L_\infty$ performance level $\gamma$ for different $d_2$.

| $d_2$ | 0.1 | 0.3 | 0.5 | 0.7 | 1.0 |
|-------|-----|-----|-----|-----|----|
| $\gamma$ | 0.0012 | 0.0254 | 0.0398 | 0.0478 | 0.1563 |

**TABLE 2.** Minimum $L_2 - L_\infty$ performance level $\gamma$ for different $\mu_1$.

| $\mu_1$ | 0.01 | 0.1 | 0.3 | 0.5 | 0.7 |
|---------|-----|-----|-----|-----|----|
| $\gamma$ | 0.2682 | 0.3721 | 0.4168 | 0.4933 | 0.5267 |

Based on the ETCS and network environment, the network induced delay is fully investigated in the filter error system (20). In this part, the MAUB $d_2$ for guaranteeing the
stability of the error system (20) is essential. By this way solving Theorem 2, we can obtain the minimum $L_2 - L_{\infty}$ performance index for various $d_2/\mu_1$, and it is summarized in Table 1 and Table 2. From Table 1 and Table 2, we can see that the effects of the upper bound $d_2/\mu_1$ on the $L_2 - L_{\infty}$ performance index $\gamma$. Example 2: Consider the following T–S fuzzy system.

$$\dot{x}(t) = \sum_{i=1}^{2} u_i(s(t)) [A_{0i}\hat{x}(t) + A_{1i}\hat{x}(t - d(t))] + B_iw(t),$$

$$\ddot{y}(t) = \sum_{i=1}^{2} u_i(s(t))[C_i\hat{x}(t)],$$

$$z(t) = \sum_{i=1}^{2} u_i(s(t))[E_i\hat{x}(t)].$$

where

$$A_{01} = \begin{bmatrix} -2.1 & 0.1 \\ 1 & -1 \end{bmatrix}, \quad A_{02} = \begin{bmatrix} -2 & 0 \\ -0.2 & -1.1 \end{bmatrix},$$

$$A_{11} = \begin{bmatrix} -1 & 0.1 \\ -0.8 & -0.9 \end{bmatrix}, \quad A_{12} = \begin{bmatrix} -0.9 & 0 \\ -1 & -1.8 \end{bmatrix},$$

$$B_1 = \begin{bmatrix} 1 \\ -0.2 \end{bmatrix}, B_2 = \begin{bmatrix} 0.6 \\ 0.3 \end{bmatrix}, C_1 = \begin{bmatrix} 1 & 2 \end{bmatrix},$$

$$C_2 = \begin{bmatrix} 1 & 0.5 \end{bmatrix}, E_1 = \begin{bmatrix} 0.5 & -2 \end{bmatrix},$$

$$E_2 = \begin{bmatrix} -0.3 & 0.3 \end{bmatrix}, u_1(s(t)) = \sin^2 t, \quad u_2(s(t)) = \cos^2 t,$$

$$w(t) = \begin{cases} 1, & 5 \leq t < 10 \\ -1, & 15 \leq t < 20 \\ 0, & \text{else} \end{cases}.$$

According to the above parameters and let $0.4 \leq d(t) \leq 0.5, v = 0.3$. By using LMIs in Corollary 1 and MATLAB LMI toolbox, then the related trigger matrix $\phi = 8.3242$ and the subsequent matrices can be derived as follows.

$$A_{f1} = \begin{bmatrix} -8.1245 & -3.3252 \\ -2.3214 & -7.5463 \end{bmatrix}, B_{f1} = \begin{bmatrix} -2.1025 \\ -0.9425 \end{bmatrix},$$

$$C_{f1} = \begin{bmatrix} 1.7458 & 0.8712 \end{bmatrix}, A_{f2} = \begin{bmatrix} -10.4752 & -2.1024 \\ -4.1204 & -9.2867 \end{bmatrix},$$

$$B_{f2} = \begin{bmatrix} -0.8412 \\ -0.7458 \end{bmatrix}, C_{f2} = \begin{bmatrix} 0.4785 & 0.1025 \end{bmatrix}.$$

Based on the zero initial condition, the state trajectories of $\xi(t)$ is depicted in Figure 3a, the corresponding simulation curves of the system states $\tilde{x}_1(t), \tilde{x}_2(t)$ and the state responses of the filters $\tilde{x}_1(t), \tilde{x}_2(t)$ are shown in Figures 3b and 3c. Figure 3d demonstrates the responses of filtering error $z(t) - \bar{z}(t)$ and the triggering instants are picturized in Figure 3e. Figure 3f depicts the corresponding state responses for the fuzzy filtering error system with different initial values. Furthermore, by solving LMIs in Corollary 1, we obtain the maximum allowable upper bounds of $d_2$ for various values of $v$, when $d_1 = 0.1$ (listed in Table 3), which clearly shows the effectiveness of our work. In addition, compared with the results of the proposed ETCS and the ETCS in [19], to show the performance of our proposed method. Figure 3e presents the transmission instants and intervals under the proposed ETCS. Furthermore, the transmission trigger times during the interval (0, 35) of the proposed ETCS is 35 release instants. One can check that the proposed ETCS released less transmitted data than those in [19], which means the energy consumption is effectively reduced. In addition, Corollary 1 obtained here are not only less conservative results but has effectively saved the limited communication resources greatly under the release intervals in Figure 3e. In conclusion, all the simulation results have indicated our theoretical analysis for the proposed algorithmic filter.

| $d_1$ | $v$ | 0.1 | 0.3 | 0.5 | 0.55 |
|-------|----|-----|-----|-----|------|
| [19]  | -  | -   | 0.4000 | -  |
| Corollary 1 | 0.5626 | 0.5421 | 0.4521 | 0.3914 |
The panels (3a)-(3f) contain the behavior of state trajectories and triggered instants in example 2.

**FIGURE 3.** The panels (3a)-(3f) contain the behavior of state trajectories and triggered instants in example 2.

**V. APPLICATION**

Example 3: Consider the tunnel diode circuit in [46] is considered to shown the performance of the proposed approach.

\[
\begin{align*}
C\dot{v}_c(t) &= -0.002v_c(t) - 0.01v_c(t)^3 + i_L(t), \\
y(t) &= v_c(t), \\
L\dot{i}_L(t) &= -v_c(t) - R i_L(t) + w(t),
\end{align*}
\]  

(59)

where \(v_c(t)\) noted as voltage of the capacitor, \(i_L(t)\) denotes the current of the inductor, \(w(t)\) indicates the disturbance, \(y(t)\) is the sampled-data measurement output. Furthermore, we initiate the parameters of the capacitor, inductor and resistance \(C = 20mF, L = 1000mH\) and \(R = 10\Omega\), respectively.

For instance, \(v_c(t) \in [-3, 3]\), the tunnel diode circuit can be described in the following fuzzy system with \(\hat{x}(t) = [\hat{x}_1(t) \hat{x}_2(t)]^T = [v_c(t) i_L(t)]^T\) and \(z(t) = \hat{x}_1(t)\).

\[
\begin{align*}
\dot{\hat{x}}(t) &= \sum_{i=1}^{2} u_i(s(t)) [A_i(t)\hat{x}(t) + B_i(t)w(t)], \\
\dot{\hat{y}}(t) &= \sum_{i=1}^{2} u_i(s(t)) [C_i(t)\hat{x}(t)].
\end{align*}
\]

Moreover, to illustrate that the effectiveness of the full-order event-triggered \(L_2 - L_\infty\) filter design approach developed in Corollary 1, the responses of \(\hat{x}(t)\) and \(\hat{y}(t)\) can be achieved by iterative estimations from initial value \(\hat{x}(0) = x_f(0) = [0 0]^T\), and the error can be easily obtained by \(e(t) = z(t) - \hat{z}(t)\) and the disturbance is considered as \(w(t) = \exp(-0.1t)\sin(0.1t)\). The evolution’s of \(\xi(t), \hat{x}(t), \hat{y}(t)\) and \(e(t)\) are shown in Figures 5a, 5b, 5c and 5d. Figure 5f shows the related state trajectories for the fuzzy filtering error system with various initial conditions. With the above simulation results that the filtering error system (60) is asymptotically stable by applying the designed parameters. The transmission instants and intervals are presented in Figure 5e. In order to satisfied the \(L_2 - L_\infty\) performance, the period is taken.
as $t \in (0, 25]$ in Figure 5e, which shows that the required transmission can save network resources. Moreover, from Figures 5a-5e, one can check ETCS cannot just mitigate the issue of resource constraints but also make the data in the transmission process faster and more stable. The triggering threshold can be chosen accordingly to the real system application requirements. Under the network communication parameters $\nu = 0.08$ and $\delta = 0.9$, therefore we get the minimum value of $L_2 - L_\infty$ performance $\gamma = 1.0254$. From the above simulation results and discussions, we can clearly illustrate that the filtering errors can achieve ultimate $L_2 - L_\infty$ performance under the designed event-triggered scheme in this paper, and it is consistent with our theoretical results.

\begin{figure}
\centering
\includegraphics[width=\textwidth]{figure5.png}
\caption{Behavior of the responses for various states $\hat{x}(t), \hat{x}_1(t), x_f(t), \dot{x}_2(t), \dot{x}_f(t), e(t)$ and triggered instants in example 3.}
\end{figure}

\begin{table}
\centering
\caption{Maximum allowable bound $\nu$ and $\delta$ for example 3.}
\begin{tabular}{l|l|l}
\hline
Methods & \cite{41} & Example 3 \\
\hline
$\nu$ and $\delta$ & $\nu = 0.06$ and $\delta = 0.8$ & $\nu = 0.08$ and $\delta = 0.9$ \\
\hline
\end{tabular}
\end{table}

Example 4: As illustrated in \cite{47}, the partial element equivalent circuit (PEEC) model in Fig. 4(b) includes new circuit elements which involve retarded mutual coupling between the partial inductances of the form $L_{ij}(t - h_2)$ and retarded dependent current sources of the form $p_{ij}/\nu_{ij}(t - h_2)$. The general form of modeling PEEC can be modeled as

\begin{equation}
C_0 \dot{x}(t) + G_0 \dot{x}(t) + C_1 \dot{x}(t - h_2) \\
+ G_1 \ddot{x}(t - h_2) = Bu(t, t - h_2), t \geq t_0; \\
\ddot{x}(t) = \phi(t), t \leq t_0.
\end{equation}

To consider the asymptotic stability of the system with the mathematical deduction, the PEEC (61) can be rewritten as the following neutral system \cite{17}:

\begin{equation}
\dot{x}(t) = A_0 \dot{x}(t) + A_1 \ddot{x}(t - h_2) + A_2 \ddot{x}(t - h_2), \\
\dot{x}(t) = \phi(t), t \leq t_0.
\end{equation}

If we take different time-varying delays into account, a more general form of PEEC (62) can be described by the following system \cite{17}

\begin{equation}
\dot{x}(t) = A_0 \dot{x}(t) + A_1 \ddot{x}(t - d(t)) + A_2 \ddot{x}(t - h(t)), \\
\dot{x}(t) = \phi(t), t \leq t_0.
\end{equation}

where the system parameters are given as \cite{17}

\begin{equation}
A_0 = \begin{bmatrix}
-2.105 & 1 & 2 \\
3 & -9 & 0 \\
1 & 2 & -6
\end{bmatrix}, \\
A_1 = \begin{bmatrix}
1 & 0 & -3 \\
-0.5 & -0.5 & -1 \\
-0.5 & -1.5 & 0
\end{bmatrix}, A_2 = \frac{1}{72} \begin{bmatrix}
-1 & 5 & 2 \\
4 & 0 & 3 \\
-2 & 4 & 1
\end{bmatrix}.
\end{equation}

Let us choose time varying delays $0.1 \leq d(t) \leq 0.8$, $0.1 \leq h(t) \leq 0.7$, $\mu_1 = 0.5$, $\mu_2 = 0.5$. Then by utilizing the above values and calling the MATLAB LMI toolbox, solving the LMI in Corollary 2, it is found that the system (54) is asymptotically stable and the state trajectories of the dynamical system converge to the zero equilibrium point with an initial state $[1.5, -0.4, -0.3]^T$ shown in Figure 7.
Remark 5: Consider the delayed neutral type system (54) with the input matrices as in [48] (Example 1). Solving the system (54), using the LMI in Corollary 2 and assume that $\mu_2 = 0$, we obtain the MAUB $d_2$ for different $d_1$ and $\mu_1$ as shown in Table 5, which clearly shows the effectiveness of our work. The results obtained in this paper are significantly better than those in [48].

| $d_1$ | Methods | $\mu_1 = 0.5$ | 0.7 | 0.9 |
|------|---------|---------------|-----|-----|
| 0.5  | [48]    | 2.096         | 1.811 | 1.810 |
| 1.5  | Corollary 2 | 2.121         | 1.922 | 1.910 |

VI. CONCLUSION

To conserve network bandwidth, we presented an event-triggered $L_2 - L_\infty$ filtering for network-based neutral systems via T-S fuzzy approach. Using a new ETCS and the suitable LKF, Wirtinger’s inequality technique, we established some sufficient conditions and constructed the LMIs to ensure the asymptotic stability of the filtering error system. The numerical examples demonstrate how the proposed communication scheme will greatly reduce network bandwidth consumption while maintaining the desired efficiency of the filtering error system. Moreover, the model proposed in this work can be also extended event-triggered mechanism to the discrete time domain with imperfect communication, such as packet dropouts and quantization. We will also target on the complex phenomena like the randomly occurring uncertainties, incomplete measurements, general switching system with repeated scalar nonlinearities, T–S fuzzy based piecewise Lyapunov function and event-triggered with asynchronous sampling, which makes the model more practical and will be investigated in our future work.

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