High-Performance 3-Phase 5-Level E-Type Multilevel–Multicell Converters for Microgrids

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Abstract: This paper focuses on the analysis and design of two multilevel–multicell converters (MMCs), named 3-phase 5-Level E-Type Multilevel–Multicell Rectifier (3Φ5L E-Type MMR) and 3-phase 5-Level E-Type Multilevel–Multicell Inverter (3Φ5L E-Type MMI) to be used in microgrid applications. The proposed 3-phase E-Type multilevel rectifier and inverter have each phase being accomplished by the combination of two I-Type topologies connected to the T-Type topology. The two cells of each phase of the rectifier and inverter are connected in interleaving using an intercell transformer (ICT) in order to reduce the volume of the output filter. Such an E-Type topology arrangement is expected to allow both the high efficiency and power density required for microgrid applications, as well as being capable of providing good performance in terms of quality of the voltage and current waveforms. The proposed hardware design and control interface are supported by the simulation results performed in Matlab/Simulink. The analysis has been then validated in terms of an experimental campaign performed on the converter prototype, which presented a power density of 8.4 kW/dm 3 and a specific power of 3.24 kW/kg. The experimental results showed that the proposed converter can achieve a peak efficiency of 99% using only silicon power semiconductors.

Keywords: multilevel–multicell converter; wide bandgap devices; high performance; interleaved topology; power density; specific power; microgrid

1. Introduction

The electrical power demand has increased in all applications, such as transportation, industry, household, and the commercial sectors [1]. We are in fact becoming more and more hungry for electric power: on one hand, this is provoked by the constant increase in the world population, and consequently the urban centers are increasing in size with more people living in cities; on the other hand, the hunger for energy, especially in developing countries always in need of new infrastructure such as hospitals, schools, and transport, comes from the middle class. Thus, the increased demand of energy should be addressed by both significantly increasing the use of renewable energy sources and improving the efficiency of energy systems [2]. Currently, the most abundant renewable energy sources are wind and solar [3,4]; for both of them, adequate conversion equipment is needed. For example, wind energy requires turbines and generators, which leads to variable frequency and variable voltage electricity. As a result, between the generator and the grid, a power conversion system is needed in order to meet the grid requirement of a fixed frequency of 50 or 60 Hz at certain standard voltage levels. Concerning solar energy, a photovoltaic (PV) cell provides a DC source at unregulated low voltage, and thus power electronics systems must be able to adjust this DC voltage level to one suitable for supplying the load [5]. In the 21st century, therefore, modern solutions based on different energy sources coming from wind, solar, energy storage and micro-turbines have been used to feed the load or different loads [6,7]. Particularly, in a stand-alone microgrid, more energy sources are connected to...
The photovoltaic system and the battery system are connected to the DC-bus thanks to a DC/DC power converter [8,9], while the wind system and the micro-turbine are connected to the DC-bus through an AC/DC converter. The power flows from the DC-bus to the load thanks to the DC/AC converter connected to a power filter.

**Figure 1.** Structure of stand-alone microgrid with the integrated renewable energy source.

It is evident that the modern renewable energy system could not operate, and the microgrid could not be realized, without power electronics. In fact, power electronics converters and controllers are the most important elements in this application, and the efforts of power conversion designers consistently focuses on improving the efficiency and reducing the volumes of the conversion system [10,11]. These goals can be reached thanks to the continuous improvement of power electronics technologies and power converter topologies. Indeed, on one hand the industrial manufacturing of power components keeps introducing new high-performance modules and power semiconductors on the market [12,13]; on the other hand, newer and emerging power converter topologies are constantly proposed in literature. For example, in high power and/or high voltage applications, the limit of the power conversion system is attributed to the power semiconductors capable of withstanding limited voltage and current stresses. To overcome this problem, academia and industry are working on new solutions of power converters [14–16]. Thus, the use of multilevel configurations allows the arrangement of power conversion systems with power semiconductors that are required to withstand only a fraction of both the overall DC-bus voltage and the converter output current. This usually allows higher switching frequency $f_{sw}$ and, therefore, multilevel configurations lead to significant improvements in terms of quality of both voltage and current waveforms without giving up the benefit of high efficiency and high-power density. Furthermore, the weight and volume of the converter passive components are likely to be reduced [14–17], which is very appealing for several applications, where the overall size and weight of the electrical generating system needs to be minimized. Given the high number of benefits, more and more multilevel converter topologies are proposed in the literature [17–21]. It is understood that multilevel topology can act on the voltage stress of the power semiconductors, leaving their current ratings unchanged. To reduce the current stress flowing through the power semiconductors, more parallel cell converters can be used. Thus, the power semiconductors with low current rating can be chosen, leading to an improvement in the conduction losses. As another ad-
vantage, parallel converters enhance the current ripple, resulting in a further improvement of the waveform quality. Obviously, the multilevel converters present some disadvantages, such as the reliability and cost. In fact, the number of power semiconductors in multilevel converters increases as the number of the voltage levels increases, and, therefore, we could think that cost and reliability worsen. However, some multilevel topologies proposed in the literature have fault tolerance capability [22–24]. Additionally, even if the number of power devices increases, there is a reduction in passive devices, which leads to less use of copper and iron. These materials, actually, are more expensive than power semiconductors. Naturally, the real disadvantage of having many devices could lie in the driver circuits used for switching the devices [25]. Moreover, tuning the control algorithm could also be more complicated, given the difficulty in finding an analytical model of the multilevel converter [26,27]. Nevertheless, apart from the analytical effort required to find the control law, the continuous trend of increasing the controller performance and memory size along with the reduction in the cost has now reached a point where the increase in the number of power semiconductors is not such a disadvantage. Multilevel converters based on Neutral Point Clamped (NPC) and T-Type topologies have been proposed using Super-junction MOSFETs [17,18]. Here, the peak efficiency is estimated to be above 99%. A five-level T-Type converter able to reach an efficiency of 99.2% using only SiC technology is presented in [19]. In this paper, the confirmed power density and specific power are 1.4 kW/dm$^3$ and 2.5 kW/kg. In [20] a three-phase T-Type converter, called Swiss Rectifier, has been designed using SiC power devices. The declared peak efficiency and power density were 99.26% and 4 kW/dm$^3$, respectively. A hybrid Five-Level Active NPC Inverter that uses SiC and is able to achieve a peak efficiency above 98% has been proposed in [21].

One of the goals of the proposed paper is analyzing, designing, and testing the $3\Phi 5$L E-Type MMR and the $3\Phi 5$L E-Type Multilevel–Multicell Inverter (MMI) to obtain high efficiency, power density and specific power by using only silicon (Si) power semiconductors. For this purpose, the operation modes of the proposed converters are clearly explained and a solution to balance the DC-bus voltages is discussed. Then, the investigation focused on the design of the proposed converters; an analytical approach to calculate the device stress is presented to select the suitable power semiconductors. Starting from this analysis, the power semiconductors have been selected and the efficiency as a function of the power has been analytically calculated for both converters. The theoretical investigation has been supported by the model of the converters created in the Matlab/Simulink and Plexim/Plecs environments. A prototype of the converters has been built and the proposed MMR and MMI are integrated on the same power board to reduce the power density. Furthermore, the control structures for both MMR and MMI to be used in microgrid applications have been implemented and verified through preliminary simulations. Finally, experimental tests have been performed in order to confirm the obtained theoretical analysis. This paper is organized as follows: the topology, the operation principle, and the voltage unbalancing issue of the $3\Phi 5$L E-Type MMR and $3\Phi 5$L E-Type MMI are presented in Section 2. The hardware aspect design of the proposed rectifier and inverter are illustrated in Section 3. Based on the proposed rectifier and inverter, the control strategies regarding stand-alone microgrid applications have been discussed in Section 4. Simulation results and experimental results from a laboratory prototype are shown in Sections 5 and 6, respectively. Conclusions are presented in Section 7.

2. Operation Structure of 3-Phase 5-Level E-Type MMC

2.1. 3$\Phi$5L E-Type MMR and MMI

The circuit of the $3\Phi 5$L E-Type MMR is illustrated in Figure 2. A single-phase of the rectifier has two cells: cell 1 and cell 2. This converter is based on both $I$-Type and $T$-Type topology [28–30]. In fact, each cell is composed of two I-Type legs connected to the T-Type leg. The power flows in one direction in the $3\Phi 5$L E-Type MMR due to the presence of the diode into the T-Type cell. The two cells are connected in an interleaving manner, using an intercell transformer (ICT). The advantages of paralleling the cells using the ICT lies in the
fact that the phase current is equally shared between the cells, the amplitude of the total current ripple is reduced, and the harmonic contents of the voltage at high frequency is shifted at twice the switching frequency. The 3Φ5L E-Type MMI is also composed of the I-Type and T-Type topologies like the rectifier, as illustrated in Figure 3. Each phase has two cells connected through the ICT.

![Figure 2. Circuit of 3Φ5L E-Type Multilevel–Multicell Rectifier (MMR).](image)

![Figure 3. Circuit of 3Φ5L E-Type Multilevel–Multicell Inverter (MMI).](image)

According to the modulation control scheme, both converters show five voltage levels on a single cell, while each phase has nine voltage levels, as shown in Figures 4 and 5. Thus, the line-to-line voltage shows seventeen voltage levels. A carrier-based pulse width modulation (PWM) method has been implemented, taking into account the multiple power semiconductors of the converters. The gate signals of the power devices are generated by the comparison of the modulating signals with the carriers, as shown in Figure 6. Considering the interleaving concept, a phase displacement is applied between the parallel cells in order to achieve highest quality of the output waveforms. Thus, four carrier signals, \(c_{111}, c_{112}, c_{113}\) and \(c_{114}\) (solid line) control the power devices in cell 1, and the other carrier signals \(c_{121}, c_{122}, c_{123}\) and \(c_{124}\) (dashed line) in the opposite phase control the power semiconductors in cell 2. Furthermore, as can be seen from Figure 6, two devices are controlled by a single carrier signal. The switching frequency of each power semiconductors is \(f_{sw}\) while the output waveform effective switching frequency is
twice $f_{sw}$. This phenomenon, present in the interleaved converters, is usually called the multiplicative effect of the effective switching frequency, and leads to a drastic reduction in the output filter.

**Figure 4.** Phase-to-neutral switching voltage $u_{a1(sw)}$ (or $u_{a2(sw)}$).

**Figure 5.** Line-to-line switching voltage $u_{a(sw)}$ (or $u_{u(sw)}$).

**Figure 6.** Modulation control scheme for power semiconductors located in a single-phase of the inverter.
2.2. Balancing Circuit

The main problem of the multilevel converter based on T-Type or E-Type topologies is the unequal voltage across the DC-bus capacitors [31–33]. This problem cannot be solved in a simple way with a control algorithm due to the uncontrollable current flow through the internal nodes [28] of the capacitors. The only chance to balance the DC-bus capacitors of the 3Φ5L E-Type converters is to use an external circuit. The focus of this paper was not to study the unbalanced voltage capacitor problem. Here, two series resonant balancing circuits (SRBCs) have been used to solve the voltage unbalancing problem. Figure 7 illustrates the circuit and the implemented prototype of the SRBCs.

The SRBCs were built with four Semitop3 SK75GB066T modules (rated 60 A—600 V), 4 µH and 16 µF as resonant total inductance (\(L_{R1}/L_{R2}\)) and total capacitance (\(C_{R1}/C_{R2}\)), respectively. Furthermore, one DC-bus film capacitor and two DC-bus electrolytic capacitors were used as a DC link. The energy was transferred from the capacitor \(C_{B1}\) to \(C_{B2}\) and from the capacitor \(C_{B3}\) to \(C_{B4}\) through the capacitors \(C_{R1}\) and \(C_{R2}\). The auxiliary inductors \(L_{R1}\) and \(L_{R2}\) were used to achieve a zero-current switching (ZCS) condition. The power semiconductors were driven with complementary control signals with a constant duty cycle at 50%; no control loops and sensors were required with the system being self-balanced. These two SRBCs were used to balance the voltage across the capacitors to ensure equal DC currents \(i_{C1} = i_{C2} = i_{C3} = i_{C4}\).

3. Hardware Design and Prototype of E-Type Topology

The 3Φ5L E-Type MMR and MMI have been designed to maximize the efficiency, power density, and specific power, without sacrificing the quality of the voltage and current waveforms. To accomplish these tasks, different actions have been carefully carried out.

The capacitors of the DC-bus have been chosen considering the maximum peak-to-peak voltage ripple \(\Delta V_{BUS}\) equal to 100 V and the estimated Root Mean Square (RMS) current flow through the capacitors in the case of an asymmetric load condition. The DC-bus current harmonics were compensated by the SRBCs except the 100 Hz component, which had to be compensated by the capacitors. For this reason, the DC-bus capacitors were selected according to (1), where \(N_S\) and \(N_P\) were the numbers of series and parallel
capacitors, and $I_{CBUS}$ was the RMS current at double fundamental frequency defined in Equation (2).

$$C_{BUS} = \frac{2\sqrt{2} N_S N_P}{(2\pi 100) \Delta V_{BUS}} I_{CBUS}$$

$$I_{CBUS|100Hz} = \frac{U_0 I_0}{\sqrt{2} V_{BUS}}$$

In (2), $U_0$ is the RMS voltage, $I_0$ is the RMS load current, and $V_{BUS}$ is the total voltage across DC-bus capacitors. According to (1) and (2), six parallel and four series electrolytic capacitors, each one equal to 220 µF; 220 V were chosen as DC-bus capacitor tanks.

The power semiconductors were carefully selected considering the maximum voltage and current stress that the power components are able to withstand. Figure 8 shows the maximum voltage stress across the power semiconductors of a single cell of the inverter and rectifier.

![Figure 8](image-url)

Figure 8. Maximum voltage stress that each cell of the E-Type Rectifier and Inverter can withstand at a steady state.

As can be seen, the switches $S_{x,21}$, $S_{x,22}$ and the diodes $D_{x,21}$, $D_{x,22}$, with $x \in \{1R, 2R\}$ and $x \in \{1I, 2I\}$, have the maximum voltage stress equal to $3/\sqrt{2} V_{BUS}$ compared to the other power semiconductors. Naturally, the overvoltage related to the commutated current must be added to this blocking voltage but, as explained in [34], the overvoltage commutation only appears when the blocking voltage at a steady state is equal to $1/4 V_{BUS}$. Concerning the current stress, the use of parallel cells helps to reduce the current stress of the power semiconductors. To obtain the current stress of each power semiconductors, an analytical procedure has been performed. Particularly, the average (AVG) and the root mean square (RMS) currents flowing in the power semiconductors located in the rectifier and inverter are expressed in Equation (3), where $M_{0R}$ is the modulation depth of the rectifier, $I_{in}$ is the RMS phase current of the rectifier, $M_{0I}$ is the modulation depth of the inverter, $I_0$ is the RMS phase current inverter, and $a_{RMS,i}$, $b_{RMS,i}$, $a_{AVG,i}$, $b_{AVG,i}$, $a_{RMS,j}$, $b_{RMS,j}$, $a_{AVG,j}$, $b_{AVG,j}$ are the coefficients related to the switches of the rectifier (i-index) and inverter (j-index). The derivation of Equation (3) requires very complex analysis, and it is beyond the scope of this
discussion. A simplified discussion to obtaining the Equation (3), including the coefficients, is discussed in detail in Appendix A.

$$i_{RMS,R}(t) = \sqrt{\frac{I_{in}^2 M_{0R}}{\pi}}\left(\frac{a_{RMS,j}}{M_{0R}} + b_{RMS,j}\right)$$

$$|i_{AVG,R}(t)| = \sqrt{\frac{2 I_{in} M_{0R}}{\pi}}\left(\frac{a_{AVG,j}}{M_{0R}} + b_{AVG,j}\right)$$

$$i_{RMS,I}(t) = \sqrt{\frac{I_{out}^2 M_{0I}}{\pi}}\left(\frac{a_{RMS,j}}{M_{0I}} + b_{RMS,j}\right)$$

$$|i_{RMS,I}(t)| = \sqrt{\frac{2 I_{out} M_{0I}}{\pi}}\left(\frac{a_{AVG,j}}{M_{0I}} + b_{AVG,j}\right)$$

(3)

Starting from this analysis, the selected power semiconductors of the 3Φ5L E-Type Rectifier and Inverter are listed in Table 1. To improve the power density and the specific power, the 3Φ5L E-Type MMR and MMI were integrated on the same power board. The power switches of the rectifier and inverter were driven by three boards, each one controlling a single-phase of the rectifier and inverter.

**Table 1.** Power semiconductors used to build the 3Φ5L E-Type MMR and MMI with $x \in \{1R, 2R\}$ and $y \in \{1I, 2I\}$.

| Device      | Part Number | Voltage Rating | Current Rating | Technology       | Manufacturer |
|-------------|-------------|----------------|----------------|------------------|--------------|
| $S_{x,11}, S_{x,12}, S_{x,31}, S_{x,32}$ | IPT210N25NFD | 250 V          | 69 A           | OptiMOST\textsuperscript{TM} 3 | Infineon     |
| $D_{x,21}, D_{x,22}$ | IDP30E120 | 1200 V         | 30 A           | Si Diode         | Infineon     |
| $S_{x,23}, S_{x,24}$ | IPL60R104C7 | 650 V          | 20 A           | CoolMOS\textsuperscript{TM} C7 |             |
| $S_{y,11}, S_{y,12}, S_{y,31}, S_{y,32}$ | IPT210N25NFD | 250 V          | 69 A           | OptiMOST\textsuperscript{TM} 3 | Infineon     |
| $S_{y,21}, S_{y,22}$ | IKW40N120H3 | 1200 V         | 40 A           | IGBT H3          | Infineon     |
| $S_{y,23}, S_{y,24}$ | IKW20N60T | 600 V          | 20 A           | Trenchstop\textsuperscript{TM} IGBT | Infineon     |

The Infineon integrated circuit (IC) (part number 1EDI60I12AF) was employed as a gate driver chip. The printed circuit boards (PCBs) of the power board and the gate driver board have been optimized to reduce the current path during the commutations; in this way, the commutation inductance, i.e., the resulting inductance in the commutation circuit, has been reduced, and with it also the overvoltage commutation.

Additionally, because the high gate driver signals result from the high number of the power switches located in the 3Φ5L E-Type MMR and MMI, the interconnecting board which routes all the signals between the diver boards to the control board has been built.

Finally, the input and output filters have been designed to reduce the volume and to obtain high quality of the input currents in the rectifier side and high quality of the output voltages in the inverter side. Thus, the input and output ICTs and the input and output inductors have been built according to the analysis proposed in [30]. The complete prototype of the 3Φ5L E-Type MMR and MMI is illustrated in Figure 9, and features a power density of 8.4 kW/dm$^3$ and a specific power of 3.24 kW/kg.
Figure 9. Prototype of the 3Φ5L E-Type Rectifier and Inverter including the input and output power filters, measuring 580 mm × 300 mm × 45 mm. The power density is 8.4 kW/dm³ and the specific power is 3.24 kW/kg.

4. Control Interface

Figure 10 shows the block scheme of the 3Φ5L E-Type MMI. This converter must be provided with sinusoidal three-phase voltage waveforms with reduced total harmonic distortion (THDv). To meet this target, a multi-resonant controller [35] has been carefully chosen. Figure 11 illustrates the control algorithm of the 3Φ5L E-Type MMR connected to the wind source or to the micro-turbine source. As can be seen, the external speed loop provides the current reference to the q-controller inner loop. The task of this controller is to regulate the phase current to reduce the THD. The ICT circulating currents are regulated by adding an offset into the modulating signals with an additional loop.

Figure 10. Block diagram of the grid-side 3Φ5L E-Type MMI control algorithm.
5. Simulation Results

The hardware design previously addressed has been verified using a simulation model realized in the Matlab/Simulink and Plexim environments. Particularly, the power converter models have been implemented in Plecs, while the control structures have been implemented in Simulink. The stress of the power semiconductors and the losses distribution have been evaluated in the Plecs environment, which has a specific domain for modeling power semiconductors. Moreover, based on the manufacturer of the power semiconductors, the 2D look-up tables and 3D look-up tables have been created in Plecs to evaluate the loss distribution. Figures 12 and 13 show the AVG and RMS current flowing into power semiconductors of the E-Type MMI and E-Type MMR for different values of the output power. Given the symmetry of the circuit, only the current flows through the power switches located in the bottom side of the E-Type MMI and E-Type MMR are illustrated. Both the analytical and experimental approaches provide the same results.

As can be seen, in the inverter side the most stressed switches are $S_{y,21}, S_{y,22}$, while the least stressed switches are located in the middle leg $S_{y,23}, S_{y,24}$. In the rectifier side, the most stressed and the least stressed power semiconductors are $D_{x,21}, D_{x,22}$ and $S_{x,23}, S_{x,24}$, respectively.
Based on the datasheet provided by the power semiconductor manufacturers, it has been possible to estimate the efficiency distribution of the proposed converters using an analytical approach and a simulation approach. Particularly, starting from the achieved AVG and RMS currents, analytical equations to estimate the losses of the converters have been obtained according to the method proposed in [36]. Numerical efficiency results from the obtained analytical equations have been compared with simulation results. Figure 14 shows the total efficiency of the 3Φ5L E-Type MMR and MMI, including the passive components, as a function of the power. These results have been obtained based on the selected power semiconductors and the operating parameters listed in Tables 1 and 2. The peak efficiency occurs when the power is close to 10 kW, while the efficiency at a nominal point is above 98%. As can be seen, the simulation results closely match the analytical results. Operation modes and characteristic waveforms of the 3Φ5L E-Type MMR and MMI have been evaluated according to the operating point listed in Table 2.

Figure 13. Comparison between the analytical and simulation approaches of the currents flowing in the power semiconductors located in the 3Φ5L E-Type MMR: (a) AVG; (b) RMS.

Figure 14. Total efficiency of the 3Φ5L E-Type MMC as a function of the power $P_r$: analytical result (green line), simulation result (orange line).


**Table 2.** Operating parameters of the 3Φ5L E-Type MMR and MMI.

|                          | 3Φ5L E-Type MMR | 3Φ5L E-Type MMI |
|--------------------------|-----------------|-----------------|
| DC-Bus voltage           | $V_{BUS} = 600$ V | $V_{BUS} = 600$ V |
| Switching frequency      | $f_{sw} = 20$ kHz | $f_{sw} = 20$ kHz |
| Fundamental frequency    | $f_{in} = 100$ Hz | $f_0 = 50$ Hz |
| Modulation depth         | $M_{QR} = 0.93$ | $M_{QR} = 0.93$ |

Figure 15 shows the output phase voltages $u_a$, $u_b$, $u_c$, the phase-to-neutral switching voltages $u_{a(\text{sw})}$, $u_{b(\text{sw})}$, $u_{c(\text{sw})}$, and the inductor phase currents $i_a$, $i_b$, $i_c$ of the 3Φ5L E-Type MMI under resistive three-phase loads. As can be seen, the voltage waveforms show a sinusoidal trend with very low total harmonic distortion.

The waveforms of the 3Φ5L E-Type MMR are illustrated in Figure 16, where it is possible to notice, from the top to bottom, the phase back electromotive force (EMF) $u_a$, $u_b$, $u_c$, the phase-to-neutral switching voltage $u_{a(\text{sw})}$, $u_{b(\text{sw})}$, $u_{c(\text{sw})}$, the cell-to-neutral switching voltage $u_{a1(\text{sw})}$, $u_{b1(\text{sw})}$, $u_{c1(\text{sw})}$, and the electrical machine phase current $i_a$, $i_b$, $i_c$.

Here, the cell-to-neutral switching voltages also show five voltage levels, while the phase-to-neutral switching voltages exhibit nine voltage level. Thanks to the combination of the proposed topology and the control algorithm, the phase currents are regulated as three-phase sinusoidal waveforms with low total harmonic distortion.
Waveforms of the 3Φ5L E-Type MMR, from top to bottom: phase back electromotive force (EMF) $u_a$, $u_b$, $u_c$, phase-to-neutral switching voltages $u_{a1\text{sw}}$, $u_{b1\text{sw}}$, $u_{c1\text{sw}}$, cell-to-neutral switching voltages $u_{a1\text{cn}}$, $u_{b1\text{cn}}$, $u_{c1\text{cn}}$, electrical machine phase currents $i_a$, $i_b$, $i_c$.

6. Experimental Results

Experimental results have been carried out on 20 kVA 3Φ5L E-Type MMC prototypes previously described to support the proposed analysis. The DC-bus voltage was kept at 600 V by one port of the multi-port Dual Active Bridge (DAB) converter available in the laboratory [9]. The 3Φ5L E-Type MMR was connected to a permanent magnet synchronous motor (PMSM) to emulate the wind source and the 3Φ5L E-Type MMI was connected to the resistive load bench. Figure 17 shows the experimental setup of the multilevel converter including the SRBCs.

As can be seen from the Figure 17, the 3Φ5L E-Type MMR and MMI were controlled using two different control boards, which were based on the National Instruments sbRIO-9651 System on Module (SoM), as shown in Figure 18. The SoM is equipped with both...
a microprocessor (µP) and a field-programmable gate array (FPGA), the control loop of the voltages or, in case of the rectifier side, the control loop of the currents and speed, run on the FPGA using 32-bit floating point arithmetic, while system managements and communication infrastructure are managed by the µP.

![Control architecture with the National Instruments sbRIO-9651 System on Module (SoM).](image)

Figure 18. Control architecture with the National Instruments sbRIO-9651 System on Module (SoM).

Figure 19 shows the phase-to-neutral switching voltage $u_{u(sw)}$, the cell-to-neutral switching voltage $u_{u1(sw)}$, the voltage waveform after the filter $u_u$, and the phase current $i_u$ under resistive load, when the fundamental frequency $f_0$ was equal to 50 Hz, the switching frequency $f_{sw}$ was equal to 20 kHz, and the modulation depth $M_0$ was equal to 0.93. Figure 19 shows the five voltage levels across the single cell converter $u_{u1(sw)}$ and nine voltage levels across the single phase $u_{u(sw)}$ for a fixed modulation index. Figure 20 shows the output voltage waveforms under resistive load. These results prove the good capability of the multi-resonant controller to perfectly track the voltage references and to compensate the harmonics introduced by dead component time.

![3Φ5L E-Type MMI waveforms, from top to bottom: phase-to-neutral switching voltage $u_{u(sw)}$, cell-to-neutral switching voltage $u_{u1(sw)}$, output voltage $u_u$ and phase current $i_u$.](image)

Figure 19. 3Φ5L E-Type MMI waveforms, from top to bottom: phase-to-neutral switching voltage $u_{u(sw)}$, cell-to-neutral switching voltage $u_{u1(sw)}$, output voltage $u_u$ and phase current $i_u$. 
Figure 21 illustrates the normalized harmonic spectrum of the phase-to-neutral voltage $u_a$. The amplitude was normalized with respect to the fundamental. The harmonics magnitude from the 15th to 50th order exhibited an amplitude less than 0.1%. The THDv valuated up to the 50th order was close to 0.88%.

Figure 20. Phase-to-neutral voltages $u_a$, $u_v$, $u_w$ of the 3Φ5L E-Type MMI side under resistive load.

Figure 22 shows the phase-to-neutral switching voltage $u_a(sw)$, the extracted fundamental component, the electrical machine phase current $i_a$, and angular position $\theta_{el}$, when the fundamental frequency $f_0$ was equal to 100 Hz, the switching frequency $f_{sw}$ was equal to 20 kHz, and modulation depth $M_{0R}$ was equal to 0.93.

Figure 21. Harmonic spectrum of the phase-to-neutral voltage $u_a$. 
using only the Si power semiconductors, and at nominal power the efficiency was above 98%. Furthermore, the experimental results showed a good matching compared to the theoretical analysis. Consequently, the achieved experimental point validated the theoretical performance analysis of the 3Φ5L E-Type MMI. 

Figure 22. 3Φ5L E-Type MMR waveforms, from top to bottom: phase-to-neutral switching voltage $u_{a(sw)}$, fundamental component (extracted), electrical machine phase current $i_a$, and angular position $\theta_{el}$. 

Here, the nine voltage levels are also clearly visible, and the control algorithm provided good tracking capability, making the machine current almost a pure sinusoidal waveform. The normalized harmonic spectrum of the phase current normalized with respect to the fundamental is shown in Figure 23. The THD of the electrical machine phase current estimated up to the 50th order was equal to 1.95%. The efficiency of the 3Φ5L E-Type Rectifier and Inverter have been evaluated by using the PM3000A wattmeter, where one channel has been used to measure the input power at the DC-bus and two channels have been used to measure the output power through Aron’s insertion. Figure 24 illustrates the experimental efficiency (blue line) of the 3Φ5L E-Type MMR plus 3Φ5L E-Type MMI including filters. As can be seen, the peak efficiency was equal to 98.81% by using only the Si power semiconductors, and at nominal power the efficiency was above 98%. Furthermore, the experimental results showed a good matching compared to the theoretical analysis. Consequently, the achieved experimental point validated the theoretical performance analysis of the 3Φ5L E-Type MMR and the 3Φ5L E-Type MMI.

Figure 23. Harmonic spectrum of the electrical machine phase currents $i_a$. 

Here, the nine voltage levels are also clearly visible, and the control algorithm provided good tracking capability, making the machine current almost a pure sinusoidal waveform. The normalized harmonic spectrum of the phase current normalized with respect to the fundamental is shown in Figure 23. The THD of the electrical machine phase current estimated up to the 50th order was equal to 1.95%. The efficiency of the 3Φ5L E-Type Rectifier and Inverter have been evaluated by using the PM3000A wattmeter, where one channel has been used to measure the input power at the DC-bus and two channels have been used to measure the output power through Aron’s insertion. Figure 24 illustrates the experimental efficiency (blue line) of the 3Φ5L E-Type MMR plus 3Φ5L E-Type MMI including filters. As can be seen, the peak efficiency was equal to 98.81% by using only the Si power semiconductors, and at nominal power the efficiency was above 98%. Furthermore, the experimental results showed a good matching compared to the theoretical analysis. Consequently, the achieved experimental point validated the theoretical performance analysis of the 3Φ5L E-Type MMR and the 3Φ5L E-Type MMI.

Figure 23. Harmonic spectrum of the electrical machine phase currents $i_a$. 

Here, the nine voltage levels are also clearly visible, and the control algorithm provided good tracking capability, making the machine current almost a pure sinusoidal waveform. The normalized harmonic spectrum of the phase current normalized with respect to the fundamental is shown in Figure 23. The THD of the electrical machine phase current estimated up to the 50th order was equal to 1.95%. The efficiency of the 3Φ5L E-Type Rectifier and Inverter have been evaluated by using the PM3000A wattmeter, where one channel has been used to measure the input power at the DC-bus and two channels have been used to measure the output power through Aron’s insertion. Figure 24 illustrates the experimental efficiency (blue line) of the 3Φ5L E-Type MMR plus 3Φ5L E-Type MMI including filters. As can be seen, the peak efficiency was equal to 98.81% by using only the Si power semiconductors, and at nominal power the efficiency was above 98%. Furthermore, the experimental results showed a good matching compared to the theoretical analysis. Consequently, the achieved experimental point validated the theoretical performance analysis of the 3Φ5L E-Type MMR and the 3Φ5L E-Type MMI.

Figure 23. Harmonic spectrum of the electrical machine phase currents $i_a$. 

Here, the nine voltage levels are also clearly visible, and the control algorithm provided good tracking capability, making the machine current almost a pure sinusoidal waveform. The normalized harmonic spectrum of the phase current normalized with respect to the fundamental is shown in Figure 23. The THD of the electrical machine phase current estimated up to the 50th order was equal to 1.95%. The efficiency of the 3Φ5L E-Type Rectifier and Inverter have been evaluated by using the PM3000A wattmeter, where one channel has been used to measure the input power at the DC-bus and two channels have been used to measure the output power through Aron’s insertion. Figure 24 illustrates the experimental efficiency (blue line) of the 3Φ5L E-Type MMR plus 3Φ5L E-Type MMI including filters. As can be seen, the peak efficiency was equal to 98.81% by using only the Si power semiconductors, and at nominal power the efficiency was above 98%. Furthermore, the experimental results showed a good matching compared to the theoretical analysis. Consequently, the achieved experimental point validated the theoretical performance analysis of the 3Φ5L E-Type MMR and the 3Φ5L E-Type MMI.
Figure 24. Total efficiency of the $3\Phi 5L$ E-Type MMC as a function of the power $P_0$: analytical result (green line), simulation result (orange line) and experimental result (blue line).

7. Conclusions

The multilevel–multicell $3\Phi 5L$ E-Type MMI and $3\Phi 5L$ E-Type MMR for stand-alone microgrid applications have been presented and discussed in this paper. The E-Type topology has been carefully studied with reference to the multicell interleaving configuration. The advantages and disadvantages of the proposed multilevel–multicell converters have been clearly explained. To build the prototype of the MMR and MMI, the hardware design process has been discussed. The prototype of the proposed multilevel-multicell has been built, aiming for improvements in the power density and specific power, as well as the power quality of the voltage and current waveforms. In fact, the complete prototype of the $3\Phi 5L$ E-Type MMR plus $3\Phi 5L$ E-Type MMI presented a power density of 8.4 kW/dm$^3$ and a specific power of 3.24 kW/kg. To evaluate the performance of the multilevel–multicell converters, the control strategies have been introduced with particular regard to stand-alone microgrid applications. Experimental results confirmed the effectiveness of the proposed multilevel–multicell converters, achieving a peak efficiency of 98.81% using Si power semiconductors, as well as a $THD_v$ of 0.88% and a $THD_i$ of 1.95%.

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Appendix A

The analytical approach is presented in this section to calculate the AVG and the RMS current flowing through the power semiconductors in the 3Φ5L E-Type MMR and MMI. In general, the AVG and RMS current over one fundamental period can be found by Equations (A1) and (A2), where \( \theta = \omega t \), \( \omega \) is the fundamental frequency, \( i \) is the sinusoidal phase current, and \( d_d \) is the duty cycle of the devices.

\[
I_{\text{RMS}} = \sqrt{\frac{1}{2\pi} \int_0^{2\pi} |i^2(\theta) \cdot d_d(\theta)| \, d(\theta)} \tag{A1}
\]

\[
I_{\text{AVG}} = \frac{1}{2\pi} \int_0^{2\pi} |i(\theta) \cdot d_d(\theta)| \, d(\theta) \tag{A2}
\]

To find the RMS and AVG currents, the duty cycles of the power semiconductors in both rectifier and inverter must be obtained. According to the modulation strategy illustrated in Figure 6, the duty cycle of the devices can be derived from Equation (A3), where \( \theta_{\text{in}} = \omega_{\text{in}} t \), \( \theta_0 = \omega_0 t \), \( \omega_{\text{in}} \) and \( \omega_0 \) the fundamental frequency of the rectifier and inverter, respectively, \( A_{\text{car}} \) is the amplitude of the carriers and \( m_{n,\text{car}} \) is the offset of the carriers, with \( n = 1, 2, 3, 4 \), and \( m_z(\theta_{\text{in}}), m_y(\theta_0) \) are the modulation index of the rectifier and inverter, respectively, defined in (A4), with \( z \in \{A, B, C\} \) and \( w \in \{IL, V, W\} \) and \( k = 0, 1, 2, 3 \).

\[
\begin{align*}
\{ \ d_{\text{rect,devices}}(\theta_{\text{in}}) &= \frac{1}{A_{\text{car}}} \left[ \left( \frac{A_{\text{car}}}{2} - m_{n,\text{car}} \right) + m_z(\theta_{\text{in}}) \right] \\
\ d_{\text{inv,devices}}(\theta_0) &= \frac{1}{A_{\text{car}}} \left[ \left( \frac{A_{\text{car}}}{2} - m_{n,\text{car}} \right) + m_w(\theta_0) \right] \\
\end{align*} \tag{A3}
\]

\[
\begin{align*}
\{ m_z(\theta_{\text{in}}) &= M_{0R} \sin(\theta_{\text{in}} - k \frac{\pi}{3}) \\
\ m_w(\theta_0) &= M_{0I} \sin(\theta_0 - k \frac{\pi}{3}) \}
\end{align*} \tag{A4}
\]

Substituting (A4) into (A3), the duty cycles for each power semiconductor in the single cell rectifier and inverter can be expressed as (A5) and (A6), where \( \alpha_{1R} = \arcsin(0.5/M_{0R}) \) and \( \alpha_{1I} = \arcsin(0.5/M_{0I}) \) are the angles between the carrier signals and the modulating signals of the rectifier and inverter, respectively. Replacing (A5) and (A6) into (A1) and (A2), and performing some algebraic manipulations, the RMS and AVG currents in each power semiconductor can be written as in Equation (3), where the coefficients \( a_{\text{RMS},\text{ii}}, b_{\text{RMS},\text{ij}}, a_{\text{AVG},\text{ij}}, b_{\text{AVG},\text{ij}}, a_{\text{RMS},\text{ij}}, b_{\text{AVG},\text{ij}}, b_{\text{AVG},\text{ij}} \) are listed in Tables A1 and A2.

\[
\begin{align*}
\ d_{S_{11}}(\theta_{\text{in}}) &= \left\{ \begin{array}{ll}
0 & \text{if } \theta_{\text{in}} \in [0, \pi], \theta_{\text{in}} \in [\pi, \pi + \alpha_1], \theta_{\text{in}} \in [2\pi - \alpha_{1R}, 2\pi] \\
1 - 2M_{0R} \sin(\theta_{\text{in}}) & \text{if } \theta_{\text{in}} \in [\pi, 2\pi - \alpha_{1R}] \\
1 & \text{if } \theta_{\text{in}} \in [0, \pi] \end{array} \right. \\
\ d_{S_{12}}(\theta_{\text{in}}) &= \left\{ \begin{array}{ll}
1 & \text{if } \theta_{\text{in}} \in [0, \pi], \theta_{\text{in}} \in [\pi, \pi + \alpha_1], \theta_{\text{in}} \in [2\pi - \alpha_{1R}, 2\pi] \\
2[1 + M_{0R} \sin(\theta_{\text{in}})] & \text{if } \theta_{\text{in}} \in [\pi, 2\pi - \alpha_{1R}] \\
0 & \text{if } \theta_{\text{in}} \in [0, \pi] \end{array} \right. \\
\ d_{D_{11}}(\theta_{\text{in}}) &= \left\{ \begin{array}{ll}
1 & \text{if } \theta_{\text{in}} \in [0, \pi], \theta_{\text{in}} \in [\pi, \pi + \alpha_1], \theta_{\text{in}} \in [2\pi - \alpha_{1R}, 2\pi] \\
0 & \text{if } \theta_{\text{in}} \in [\pi, 2\pi - \alpha_{1R}] \\
1 & \text{if } \theta_{\text{in}} \in [0, \pi] \end{array} \right. \\
\ d_{D_{12}}(\theta_{\text{in}}) &= \left\{ \begin{array}{ll}
1 & \text{if } \theta_{\text{in}} \in [0, \pi], \theta_{\text{in}} \in [\pi, \pi + \alpha_1], \theta_{\text{in}} \in [2\pi - \alpha_{1R}, 2\pi] \\
0 & \text{if } \theta_{\text{in}} \in [\pi, 2\pi - \alpha_{1R}] \\
1 & \text{if } \theta_{\text{in}} \in [0, \pi] \end{array} \right. \\
\ d_{S_{23}}(\theta_{\text{in}}) &= \left\{ \begin{array}{ll}
0 & \text{if } \theta_{\text{in}} \in [0, \alpha_{1R}], \theta_{\text{in}} \in [\pi - \alpha_{1R}, \pi] \\
1 & \text{if } \theta_{\text{in}} \in [\alpha_{1R}, 2\pi - \alpha_{1R}] \\
1 & \text{if } \theta_{\text{in}} \in [0, \pi] \end{array} \right. \\
\ d_{S_{24}}(\theta_{\text{in}}) &= \left\{ \begin{array}{ll}
1 & \text{if } \theta_{\text{in}} \in [0, \alpha_{1R}], \theta_{\text{in}} \in [\pi - \alpha_{1R}, \pi] \\
1 & \text{if } \theta_{\text{in}} \in [\alpha_{1R}, 2\pi - \alpha_{1R}] \\
0 & \text{if } \theta_{\text{in}} \in [0, \pi] \end{array} \right. \\
\ d_{S_{21}}(\theta_{\text{in}}) &= \left\{ \begin{array}{ll}
1 & \text{if } \theta_{\text{in}} \in [0, \alpha_{1R}], \theta_{\text{in}} \in [\pi - \alpha_{1R}, \pi] \\
1 & \text{if } \theta_{\text{in}} \in [\alpha_{1R}, 2\pi - \alpha_{1R}] \\
0 & \text{if } \theta_{\text{in}} \in [0, \pi] \end{array} \right. \\
\end{align*} \tag{A5}
\]
\(d_{S_{x,11}}(\theta_0) = \begin{cases} 0 & \theta_0 \in [0, \pi], \theta_0 \in [\pi, \alpha_{11} + \pi], \theta_0 \in [2\pi - \alpha_{11}, 2\pi] \\ -1 - 2M_{01} \sin(\theta_0) & \theta_0 \in [\alpha_{11} + \pi, 2\pi - \alpha_{11}] \end{cases}\)

\(d_{S_{x,11}}(\theta_0) = \begin{cases} 1 & \theta_0 \in [0, \pi], \theta_0 \in \left[\pi, \alpha_{11} + \pi\right], \theta_0 \in [2\pi - \alpha_{11}, 2\pi] \\ 2[1 + M_{01} \sin(\theta_1)] & \theta_0 \in [\alpha_{11} + \pi, 2\pi - \alpha_{11}] \end{cases}\)

\(d_{S_{x,21}}(\theta_0) = \begin{cases} -2M_{01} \sin(\theta_1) & \theta_0 \in [\pi, \alpha_{11} + \pi], \theta_0 \in [2\pi - \alpha_{11}, 2\pi] \\ 1 & \theta_0 \in [\alpha_{11} + \pi, 2\pi - \alpha_{11}] \end{cases}\)

\(d_{S_{x,22}}(\theta_0) = \begin{cases} 2M_{01} \sin(\theta_1) & \theta_0 \in [0, \alpha_{11}], \theta_0 \in [\pi - \alpha_{11}, \pi] \\ 1 & \theta_0 \in [\pi, \pi - \alpha_{11}] \\ 0 & \theta_0 \in [\pi, 2\pi] \end{cases}\)

\(d_{S_{x,23}}(\theta_0) = \begin{cases} 1 - 2M_{01} \sin(\theta_1) & \theta_0 \in [0, \alpha_{11}], \theta_0 \in [\pi - \alpha_{11}, \pi] \\ 0 & \theta_0 \in [\alpha_{11}, \pi - \alpha_{11}] \\ 1 & \theta_0 \in [\pi, 2\pi] \end{cases}\)

\(d_{S_{x,24}}(\theta_0) = \begin{cases} 1 + 2M_{01} \sin(\theta_1) & \theta_0 \in [\pi, \alpha_{11} + \pi], \theta_0 \in [2\pi - \alpha_{11}, 2\pi] \\ 0 & \theta_0 \in [\alpha_{11} + \pi, 2\pi - \alpha_{11}] \end{cases}\)

\(d_{S_{x,31}}(\theta_0) = \begin{cases} 1 & \theta_0 \in [0, \alpha_{11}], \theta_0 \in [\pi - \alpha_{11}, \pi] \\ 2[1 - M_{01} \sin(\theta_1)] & \theta_0 \in [\alpha_{11}, \pi - \alpha_{11}] \end{cases}\)

\(d_{S_{x,32}}(\theta_0) = \begin{cases} -1 + 2M_{01} \sin(\theta_1) & \theta_0 \in [0, \alpha_{11}], \theta_0 \in [\pi - \alpha_{11}, \pi] \\ 0 & \theta_0 \in [\alpha_{11}, \pi - \alpha_{11}] \end{cases}\)

### Table A1. 3Φ5L E-Type MMR power semiconductor coefficients of the RMS and AVG currents.

| \(i\) | Power Semiconductor | Coefficients |
|------|--------------------|--------------|
| 1    | \(D_{x,21}, D_{x,22}\) | \(a_{RMS,1} = 3\pi - 6\alpha_{1R} - 3\sin(2\alpha_{1R})\) \(b_{RMS,1} = 8(\cos(\alpha_{1R}) + 2)(\cos(\alpha_{1R}) - 1)^2\) \(a_{AVG,1} = 2\cos(\alpha_{1R})\) \(b_{AVG,1} = 2\alpha_{1R} - \sin(2\alpha_{1R})\) |
| 2    | \(S_{x,11}, S_{x,32}\) | \(a_{RMS,2} = 3\pi - 6\alpha_{1R} + 3\sin(2\alpha_{1R})\) \(b_{RMS,2} = -4\cos(\alpha_{1R})(\cos^2(\alpha_{1R}) - 3)\) \(a_{AVG,2} = -2\cos(\alpha_{1R})\) \(b_{AVG,2} = \sin(2\alpha_{1R}) - 2\alpha_{1R} + \pi\) |
| 3    | \(S_{x,12}, S_{x,31}\) | \(a_{RMS,3} = \frac{1}{2}(\pi - 2\alpha_{1R} + \sin(2\alpha_{1R}))\) \(b_{RMS,3} = 2[\cos(\alpha_{1R})(\cos^2(\alpha_{1R}) - 3) + \cos(\alpha_{1R}) + 2)(\cos(\alpha_{1R}) - 1)^2]\) \(a_{AVG,3} = 4\cos(\alpha_{1R})\) \(b_{AVG,3} = 4\alpha_{1R} - 2\sin(2\alpha_{1R}) - \pi\) |
| 4    | \(S_{x,23}, S_{x,24}\) | \(a_{RMS,4} = \frac{1}{2}[2\alpha_{1R} - \sin(2\alpha_{1R})]\) \(b_{RMS,4} = 2(\cos(\alpha_{1R}) - 1)^2(-\cos(\alpha_{1R}) - 2)\) \(a_{AVG,4} = 2(1 - \cos(\alpha_{1R}))\) \(b_{AVG,4} = \sin(2\alpha_{1R}) - 2\alpha_{1R}\) |
Table A2. 3Φ5L E-Type MMI power semiconductor coefficients of the RMS and AVG currents.

| i   | Power Semiconductor | Coefficients |
|-----|---------------------|--------------|
| 1   | $S_y,21$, $S_y,22$  | $a_{RMS,1} = 3\pi - 6\alpha_{11} - 3\sin(2\alpha_{11}) + 6\sin(2\alpha_{11})\cos^2(\phi_0)$  |
|     |                     | $b_{RMS,1} = -4\sin(\phi_0)^2 + 6\sin\left(\frac{\phi_0}{2}\right)\cos(\phi_0) - 2\sin\left(\frac{3\alpha_{11}}{2} + \phi_0\right) - \sin(3\alpha_{11} - \phi_0)$  |
|     |                     | $a_{AVG,1} = 4\cos(\alpha_{11})\cos(\phi_0)$  |
|     |                     | $b_{AVG,1} = 2\sin(\alpha_{11}) + \cos(\phi_0)[4\alpha_{11} - 2\sin(2\alpha_{11}) - 2\phi_0]$  |
| 2   | $S_y,11$, $S_y,32$  | $a_{RMS,2} = 6\alpha_{11} - 3\pi + 3\sin(2\alpha_{11}) - 3\sin(2\alpha_{11})\sin(2\alpha_{11})$  |
|     |                     | $b_{RMS,2} = 8\cos^2(\alpha_{11}) + 24\cos^2(\phi_0)\cos(\alpha_{11}) - 12\cos^3(\alpha_{11})\cos(\phi_0)$  |
|     |                     | $a_{AVG,2} = -2\cos(\phi_0)\cos(\alpha_{11})$  |
|     |                     | $b_{AVG,2} = \cos(\phi_0)[\sin(2\alpha_{11}) - 2\alpha_{11} + \pi]$  |
| 3   | $S_y,12$, $S_y,31$  | $a_{RMS,3} = \frac{1}{2}(\pi - 2\alpha_{11} + \sin(2\alpha_{11})\cos(2\phi_0))$  |
|     |                     | $b_{RMS,3} = \frac{1}{2}[3 - 12\cos(\alpha_{11}) + 4\cos(\phi_0) + 2\cos(2\phi_0) - 6\cos(2\phi_0)\cos(\alpha_{11}) + + 2\cos(3\alpha_{11})\cos(2\phi_0)]$  |
|     |                     | $a_{AVG,3} = 8\cos(\alpha_{11})\cos(\phi_0)$  |
|     |                     | $b_{AVG,3} = 2\sin(\phi_0) + 2\alpha_{11}\cos(\phi_0) - 2\phi_0\cos(\phi_0) - 3\sin(2\alpha_{11})\cos(\phi_0) - \pi\cos(\phi_0)$  |
| 4   | $S_y,23$, $S_y,24$  | $a_{RMS,4} = 3\pi - 3\sin(2\alpha_{11}) + 3\cos(2\phi_0)\cos(\alpha_{11})\sin(\alpha_{11})$  |
|     |                     | $b_{RMS,4} = -6 + 6\cos(\alpha_{11}) - 2\cos(2\phi_0) + 6\cos(2\phi_0)\cos(\alpha_{11}) - 4\cos(2\phi_0)\cos^3(\alpha_{11})$  |
|     |                     | $a_{AVG,4} = 2 - 2\cos(\phi_0)\cos(\alpha_{11})$  |
|     |                     | $b_{AVG,4} = -2\cos(\phi_0) + \sin(2\alpha_{11})\cos(\phi_0) - 2\alpha_{11}\cos(\phi_0) + 2\phi_0\cos(\phi_0)$  |

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