Changes in Total Friction in the Engine, Friction in Timing Chain Transmissions and Engine Emissions Due to Adding TiO₂ Nanoparticles to Engine Oil

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Abstract
The main aim of the study was to evaluate changes in total friction in the engine, friction in its timing chain transmissions and engine emissions resulting from adding TiO₂ nanoparticles to engine oil. The applicable engine oils and factors affecting their features were discussed. The drive from the crankshaft to the camshaft in an internal combustion engine is usually carried out by means of a cogged belt transmission or a chain transmission when high mileage is required without service operations. The engine performance of analyzed SI engine was obtained from the literature. The dependency of engine emission on engine operating speed was obtained using data from tests of a very similar engine under standard test conditions described in the literature. The changes in engine characteristics caused by varying internal friction conditions were estimated using the engine performance characteristic and engine friction losses, particularly in valve train chain transmission. The friction in such a chain transmission operating under oil lubrication conditions can be determined using its analytical model and measured friction torque occurring between the chain rollers and the pins. The analytical model was developed using the finite element method and additional mathematical formulas. The proposed model allowed obtaining weight and mass inertial moments of all valve train transmission components. The friction torque in contact zone chain roller–pin was obtained using the elaborated physical pendulum method for different conditions of lubrication, namely, without oil, with pure engine oil, and with engine oil containing TiO₂ nanoparticles. The engine oil SAE 10W-40 with/without dispersed 2% wt. TiO₂ nanoparticles was used during tests. The preparation process of studied oils was described. The resulted values of the friction torque in the chain transmission operating in different conditions of lubrication and changes in engine emission have been presented for tests before and after addition of TiO₂ nanoparticles into engine oil. During the measurements it was observed that the addition of 2% TiO₂ nanoparticles into engine oil reduced the total friction losses by 7–7.7%. Additionally, it was demonstrated that the timing drive and valve train generate about 14.4–18% of overall engine friction losses. Based on the results obtained from a comparative analysis of emission in the other engine with similar power characteristics, the mentioned total friction losses can change the emission of the following compounds in the analyzed SI engine: 17–19% for CO, 8–9% for CO₂, 13–17% for NOₓ, and 12–16% for HC. Such changes were dependent on the engine speed. The smallest changes in engine were registered for the rotation speed of 2500 rpm. The oil consumption in the engine and its impact on the PM emission was estimated. The additional arrangements facilitating the extrapolation of the obtained friction results to the cases of using other oils and the method of measuring the PM emission on the test stand were proposed.

Keywords TiO₂ nanoparticles · Wear · SI engine performance characteristics · Engine emission · Valve train chain transmission · Friction

1 Introduction
The combustion engines are commonly used in the most of classic and hybrid vehicles. Their operation is strictly related to the existing valvetrains which can be of cam or camless type. Each cam-type valvetrain contains one or more camshafts. They are driven from the engine crankshaft through a
cogged belt transmission or a chain transmission when high millage is required without service operations. The valvetrains in CI engines sometimes use the gear transmissions, and historically rather bevel gear can be found in old cars of collectors or in some motorcycle engines.

According to [43] chain transmissions are more durable, compact and more efficient than other timing drive systems. If chain dynamics relative to contact stresses, contact forces between various chain drive components exceeds beyond acceptable limits, it leads to vibrations, improper valve, and fuel injection timings. Thus, the chain dynamics is the leading source of aggregating noise, vibration, and harshness (NVH) issues. If designed valve and injection timings are not achieved, it reduces the volumetric efficiency of the engine and affects overall vehicle performance and fuel consumption.

The chain gear used in SI engines contains one-, two-, or three-row chain with high strength, due to the unevenness of existing loads during engine operation. Such loads additionally induce chain pulling and can cause valve timing deregulation. The vibrations and chain runout occurring during operation of chain transmission are limited using plastic guides placed on the outside of the long straight sections of the chain. The chain transmission requires the use of pre-tensioners, usually self-acting and driven by springs or drivers using pressure of oil supplied from mean oil line of an engine. Such oil can contain different additives, i.e., TiO$_2$ [33, 45], SiO$_2$ [45], and CuO [54] nanoparticles. Components of chain mating with sprockets mounted on camshaft and crankshaft, guides, and pretensioner operate under oil lubrication, providing mixed friction conditions. The aim of the study was to evaluate the effect of TiO$_2$ nanoparticles content in an engine oil on the wear and friction of chain transmission components. The next three chapters discuss consecutively friction torques and forces in chain transmission, utilized lubricants containing TiO$_2$ nanoparticles, and models used for chain transmission.

2 Tribological Aspects of the Chain Transmission

Tribological aspects of the chain transmission are mainly related to the friction torques and friction forces acting on the transmission components and their wear. They depend on the engine loading and speed, lubrication conditions, and environmental parameters, especially temperature, humidity, and pollution, particularly reaching the interior of the transmission.

According to [67], the mechanical friction losses can be up to 9% of total SI engine losses.

According to [3], the timing drive and valve train generate approx. 20% of overall engine friction losses depending on the engine speed.

According to [48], the friction caused by chain and guide or sprocket rails is mostly higher than in the case of the toothed-belt timing drive. One of the main chain drive disadvantages is that the chain drives reach higher noise level than the toothed belt. It is caused by the impact of the chain links on the sprockets. Comparing the life prediction of the two drive mechanisms, the chain timing drive is the best. Chain damages can occur rarely during engine life and the chain timing drive maintenance is not demanding. Regarding timing drive installations, there are no high differences associated with using a toothed belt or chain drive.

Pedersen [50] elaborated the simulation model of the dynamics of roller chain drives using a continuous contact force method. The model of the contact surface between the rollers and sprocket was an important issue regarding the numerical stability of the simulation program and a model with a real tooth profile proved to be superior as compared with other applied models. With this model it is possible to perform a dynamic simulation of large marine engine chain drives.

Conwell and Johnson [8] created a new test machine configuration providing more realistic chain loading and allowing link tension and roller–sprocket impact monitoring during a normal operation.

Pereira et al. [52] used a multibody methodology to address the kinematic and dynamic effects of roller chain drives. The chain itself was modeled as a collection of rigid bodies, connected to each other by revolute clearance joints. In case of the roller chain, each clearance revolute joint, representing the connection between a pair of links, was made up of the pin link/bushing link plus the bushing link/roller pair. The problem of contact initialization and its coordination with the numerical integration procedures was treated through controlling the time step size of the numerical integration algorithm in the vicinity of the impact.

Sakaguchi et al. [57] investigated a method for reducing the friction losses in the engine timing chain using multi-body dynamics simulation. The method known as the link-by-link model was employed in the simulation to enable representation of the behavior of each single link of the chain and its friction due to contact. A model considering fluctuations in camshaft torque and crankshaft rotational speed was created. This simulation was used to verify the detailed distribution of friction in each part of the chain system as well as the changes of friction in the time domain.

Dwyer-Joyce et al. [15] used a photo-elastic stress analysis technique to determine the contact stresses in an automotive chain drive tensioner. The elaborated model used a replica tensioner made from epoxy resin. The model related the chain link load to the resulting tensioner subsurface stress field. It allowed a correlation of the observed and predicted location of isochromatic fringes, and hence to evaluate the chain link load from the photo-elastic fringe pattern. For the known load the contact model allowed determination of the magnitude and location of the resulting peak stresses.
Weber et al. [78] developed the new test method to facilitate the direct measurement of the real timing chain load under the engine conditions. The measuring principle was based on a strain gauged chain link in combination with a telemetric transducer system. It allowed the continuous observation of the link force during the complete chain revolution in order to identify significant dynamic effects, which affects the noise, wear, and incorrect valve timing.

Maile et al. [35] used the CAE (computer-aided engineering) model for the timing chain drive to study the distribution of the chain loads. They are necessary both for the concept selection stage and for the development of a reliability model for the timing chain.

Takagishi and Nagakubo [71] showed that application of the longitudinal model of the load prediction accuracy was inadequate. Accordingly, a link-by-link model was created, allowing transversal vibration to be considered.

Du et al. [14] developed an MBS (multibody dynamics system) model of the balancer chain drive. Such a model included a crank train system coupled to a full balancer drive system. The latter included the chain drive, balance shafts, and water pump. The nonlinear stiffness and damping effects of the baseline compliant crank chain sprocket and its design iterations were also added to the model.

3 Properties of the Applicable Engine Oils

For the engines used in vehicles Toyota Corolla, the following oils can be used: SAE 5W-30 (synthetic: Total, Dynamax, Mobil, Elf, Vatoil, Motul, and semi-synthetic: Ravenol, Shell) and SAE 15W-40 (mineral: Liqui Moly, Ravenol) and SAE 20W-50 (mineral: Kroon Oil) [9], and also SAE 5W-40 (synthetic: Castrol, Elf, Total, Aral, and semi-synthetic: Shell), SAE 10W-40 (semi-synthetic: SWAG, Castrol, Aral, Dynamax, Kroon Oil, Febi Bilstein, Total, Elf; Shell, Motul, Ravenol, and synthetic: Liqui Moly), and SAE 30 (mineral: i.e., Liquid Moly) [24]. Their properties are shown in Table 1. The density of applicable engine oil can vary up to 3%.

For the mineral oils the kinematic viscosity can vary in range 334 ± 132 cSt, and the Viscosity Index can vary in range 129 ± 19, for semi-synthetic oils the kinematic viscosity in range 239 ± 34 cSt and the Viscosity Index in range 159 ± 9, and for the synthetic oils the kinematic viscosity in range 190 ± 36 cSt and the Viscosity index in range 171 ± 8.

4 Factors Affected Engine Oil Frictional Properties

As discussed in the review [79], engine oil frictional properties highly depend on the oil composition, particularly on base oil characteristics, additives including viscosity modifiers (VM), friction modifiers (FM) and anti-wear ones, and recently also on balanced engine oil formulations. The modern engine oils need:

- Proper selection of base oils and VMs to obtain low viscosity oils that maximize hydrodynamic lubrication,
- Use of organic friction modifiers reducing friction in boundary and mixed lubrication regimes,
- Use of metallic/Mo based FMs for extended benefits in economy of fuel and aged oil,
- Minimizing volatile P from ZDDP allowing protection of the automotive three-way catalyst system,
- Use of P-free supplemental anti-wear additives, especially Mo and/or S based, to compensate the lower levels of ZDDP in the oil.

The weighted-average SI engine oil composition was presented in [34]. Such an oil contained 6.5% wt. of ashless dispersants, 5.5% wt. of metal detergents, 1.1% wt. of ZDDP, 1.4% wt. of inhibitors, 10.9% wt. of VMs, and 77.6% wt. of base stock.

Clevanger et al. [7] studied factors in oil affecting fuel efficiency such as SAE viscosity grade, VM, detergent-inhibitor (DI) package and FM selection using the 2.3 L engine dynamometer test. The fuel efficiency was improved with a reduction in single-grade and multi-grade oil viscosity. VM selection had a significant effect on the fuel efficiency of multi-grade oils. In some cases, the difference in fuel efficiency among multi-grade oils containing different VMs was about the same as the gain in fuel efficiency from reducing SAE grade from an SAE 10W-40 to an SAE 5W-30.

During testing of journal bearings lubricated by engine oil, Schneider and Rosenberg [58] found that for the oil formulations employing either a low viscosity or a soluble FM to reduce engine friction, the high-shear viscosity highly correlates with hydrodynamic load capacity. The use of an insoluble FM resulted in a higher bearing load capacity than expected based on high-shear viscosity.

4.1 Properties of Base Oils

Base oil in engine oils can be mineral one derived from heavier hydrocarbons during the refining process or synthetic one synthesized from highly processed chemicals beyond those directly from the crude-oil refining stream. Some base oils use exploratory fluids such as ionic liquids [77] and synthetic base stocks [70]: i.e., water-based ionic liquids and some biological base oils use biodegradable base stocks [36].

The most significant performance parameter of base oils is the viscosity, both kinematic and dynamic. The oil viscosity characteristics include the sensitivity of changes in the viscosity to temperature, such as the viscosity index (VI).
Also important is the dependence of the oil viscosity on the shear rate determined by the relative velocities and film thickness between mating surfaces. Specifications for the limits on the viscosities of the oil, including the high-temperature high-shear viscosities, at low temperatures and high temperatures, are given in the Society of Automotive Engineers (SAE) oil grade classification system [22]. Oils exhibiting viscosity adjustments at high and low temperatures are considered "multi-grade" oils [22].

Friction reduction in the range between 20–30% can be obtained by increasing the temperature of the oil [21].

For mineral oils, the major classes of heavy distillates deriving from the crude oil for the lubricant are paraffinic or naphthenic hydrocarbons. Paraffinic oils can have the VI higher than 100, while naphthenic oils can show the VI between 80 and 100. Depending on the relative composition of the base oil, the VI can vary.

The American Petroleum Institute (API) designated different groups of base oils based on the level of saturates and sulfur in the oil, and the VI:

- Groups I, II, and III contain oils with increasing level of saturates (either below, or over 90%), decreasing Sr (either greater than 0.03%, or less than 0.03%), and increasing VI (between 80 and 120, or over 120).
- Group IV contains polyalphaolefins (PAOs).
- Group V contains all others, such as polyalkylene glycols and esters [22].

The modern engine oils are less and less often formulated with Group I base oils. The combination of Group I oils with Group III oils or PAOs are commonly used. However, the use of significant amounts of Group I oils

### Table 1

| Oil mark | Oil type | SAE class | API class | API group | Kinematic viscosity at 40 °C, cSt | Kinematic viscosity at 100 °C, cSt | Viscosity index | Density at 15 °C, kg m⁻³ | Ash, sulfated mass, % | Use | Kinematic viscosity at 20 °C, cSt |
|----------|----------|-----------|-----------|-----------|----------------------------------|-----------------------------------|----------------|--------------------------|---------------------|-----|---------------------------------|
| Liqui Moly | M 30 | SJ | II | 82 | 10.4 | 110 | 880 | 0.8 | + | 256 |
| Total | S | 5W-30 | SL | IV | 62.1 | 11.9 | 191 | 853 | ++ | 145 |
| Dynamax | S | 5W-30 | SL | IV | 55 | 9.5 | 167 | 850 | ++ | 139 |
| Mobil | S | 5W-30 | SN | IV | 59.8 | 10.6 | 169 | 851 | 0.8 | ++ | 148 |
| Elf | S | 5W-30 | SM | IV | 72.8 | 12.2 | 165 | 855 | ++ | 185 |
| Vatoil | S | 5W-30 | SN | IV | 72.6 | 12.3 | 168 | 850 | ++ | 183 |
| Ravenol | PS | 5W-30 | SM | IV | 65.3 | 11.1 | 162 | 855 | 1.1 | ++ | 166 |
| Shell | PS | 5W-30 | SL | III | 70.82 | 12.18 | 171 | 853 | ++ | 177 |
| Castrol | S | 5W-40 | SN | IV | 84 | 14 | 173 | 842 | 1.22 | ++ | 212 |
| Elf | S | 5W-40 | SN | IV | 90 | 14.7 | 172 | 855 | ++ | 230 |
| Total | S | 5W-40 | SN | IV | 87 | 14 | 166 | 854 | ++ | 225 |
| Shell | PS | 5W-40 | SL | III | 82.5 | 14.4 | 182 | 860 | ++ | 202 |
| Aral | S | 5W-50 | SN | IV | 82 | 13.9 | 174 | 848 | ++ | 205 |
| SWAG | PS | 10W-40 | SL | III | 94 | 14 | 148 | 871 | ++ | 256 |
| Castrol | PS | 10W-40 | SL | III | 95.57 | 14.33 | 155 | 863 | ++ | 259 |
| Aral | PS | 10W-40 | SL | III | 92.8 | 14.07 | 156 | 861 | ++ | 250 |
| Dynamax | PS | 10W-40 | SM | IV | 86.2 | 13.7 | 156 | 866 | ++ | 225 |
| Kroon Oil | PS | 10W-40 | SF | III | 97.5 | 14.7 | 154 | 852 | ++ | 263 |
| Felt | PS | 10W-40 | SL | III | 93.8 | 13.7 | 148 | 871 | ++ | 259 |
| Bilstein | Total | PS | 10W-40 | SN | IV | 97 | 14.5 | 155 | 874 | ++ | 263 |
| Elf | PS | 10W-40 | SL | III | 96.81 | 14.81 | 160 | 873 | ++ | 258 |
| Shell | PS | 10W-40 | SM | IV | 92.1 | 14.4 | 162 | 880 | ++ | 243 |
| Motul | PS | 10W-40 | SL | III | 100.8 | 15.1 | 157 | 864 | ++ | 272 |
| Ravenol | PS | 10W-40 | SN | IV | 96.4 | 14.6 | 157 | 862 | ++ | 259 |
| Liqui Moly | S | 10W-40 | SL | IV | 88.2 | 14 | 163 | 870 | ++ | 230 |
| Ravenol | M | 15W-40 | SL | III | 105.7 | 14.3 | 138 | 870 | ++ | 307 |
| Liqui Moly | M | 15W-40 | SL | III | 91.1 | 13.7 | 152 | 880 | ++ | 247 |
| Kroon Oil | M | 20W-50 | SF | III | 159 | 17.3 | 117 | 888 | ++ | 528 |
becomes problematic due to their high volatility and high levels of S.

Therefore, the more common practice is to use exclusively Group II oils.

The high quality or top tier lubricants need the use of Group III oils and PAOs.

During current study the synthetic Liqui Moly SAE10W-40 engine oil has density equal 870 kg/m³ measured at 15.6 °C. Its kinematic viscosity at 40 °C was equal to 88.2 cSt, and at 100 °C was equal to 14 cSt. The viscosity index was equal to 163. The sulfated ash mass was of 0.8%.

According to [6], the change of the engine oil from SAE 30 to SAE10W-30 resulted in 7.3% increase of viscosity at 100 °C and 1.2% increase of fuel consumption. The change from the SAE 30 to the SAE 10W-40 resulted in 24.4% decrease of viscosity at 100 °C and 1.2% increase of fuel consumption. The change from the SAE 30 to the SAE 20W-50 resulted in 67.5% decrease of viscosity at 100 °C and 0.4% decrease of fuel consumption. When additionally high shear rate of 10⁶ 1/s occurs, such changes result in the same changes in fuel consumption, but 26.8% increase of viscosity for the SAE 10W-30, 6.5% increase of viscosity for the SAE 10W-40, and 23.6% decrease of viscosity for the SAE 20W-50 engine oil.

4.2 Types of Additives in Engine Oil

Engine oil contains typically 10–15 additives improving its properties or performance [74]. The most common engine oil additives are dispersants, detergents, anti-wear additives (AW), antioxidants, FMs, corrosion inhibitors, rust inhibitors, pour point depressants and VMs. There are some reviews covering antioxidants, corrosion inhibitors, VMs, FMs and anti-wear additives [40].

According to [4] engine oils contain zinc dialkyldithiophosphate (ZDDP) for anti-wear protection, alkali, and/or alkali earth metal sulfonate or phenate detergents neutralizing acidic combustion products, and succinic anhydride-based functionalized dispersants solubilizing oxidation products and friction modifiers, specifically molybdenum dithiocarbamate (MoDTC) and glycerol monooleate (GMO, an organic friction modifier).

The VMs, FMs, and AWs are the most important, due ability to prevent premature wear and reduce friction improving the fuel economy. Many AWs and FMs contain metallic, S and P chemistries that can adversely affect the emission after-treatment system operation.

4.3 The Role of Viscosity Modifiers

VMs are high molecular-weight polymers, added in small amounts to the base oil to reduce the temperature sensitivity of oil viscosity. This group of polymers consists of olefin copolymers (OCP), polymethacrylates (PMA), conventional and star hydrogenated styrene-isoprene copolymers, and styrene-butadiene co-polymer. Some of them exhibit also supplemental dispersing properties [59, 74]. A high VM is needed to achieve proper behavior of engine oils in wide range of values of the operating temperature, due to suppressing oil viscosity changes with the temperature. VMs must have enough shear stability in order to prevent their degradation and losing of their effectiveness during use. For example, the PAMA dispersant VMs allowed reduction of friction in the boundary and hydrodynamic lubrication regimes [44].

According to [39], there are two types of viscosity grade: mono-grade and multi-grade. Mono-grade oils, such as SAE 30, provide engine protection at normal operating temperature, but can lack fluidity at colder temperatures. Multi-grade oils commonly use VMs to achieve more flexibility and can be identified by a viscosity range, such as SAE 10W-30. The letter “W” designates that an oil can perform in both cold weather as well as at normal engine operating temperatures.

SAE 5W-30 multi-grade viscosity grade engine oil operates as a SAE 5 viscosity grade in the winter, and as a SAE 30 viscosity grade in the summer.

Mono-grade oils, such as SAE 30 and 40 grades do not contain polymers to modify the viscosity with temperature. The use of multi-grade engine oil, containing viscosity modifiers, allows the dual benefits of ease of oil pumping and starting while maintaining high temperature protection from excessive engine oil thinning.

4.4 The Role of Friction Modifiers

FMs in engine oils reduce friction in the mixed or boundary lubrication regimes. They form on mating surfaces the protective layers having very low shear strength, and thus a low friction coefficient.

There are two types of FMs used in engine oils. The first group consists of organic FM, such as oleamide, boronated ester/amides, and glycerol mono-oleate (GMO) [29]. They are the surface active FMs containing long-chain hydrocarbon molecules with polar heads anchoring to the metal surface and producing chemical film reducing friction. The second group consists of metallic FMs, such as molybdenum dithiocarbamates, trinuclear organo-molybdenum compounds, molybdate esters and molybdenum thiophosphates [66]. They are the chemically reactive FMs containing organo-metallic molecules reacting with the metal surface and producing a tribofilm reducing friction at the proper temperature range. Under certain conditions they can improve an oxidation control and wear protection. This makes the organomolybdenum-based
Emiss. Control Sci. Technol. (2020) 6:358–379

FM multi-functional. Organo-molybdenum compounds can be also used exclusively as antioxidants or AWs [19, 80]. The poor solubility of organo-molybdenum compounds in finished engine oils systems limits their applicability. Such a phenomenon prevents the formation of a stable engine oil additive system. Additionally, molybdenum dithiocarbamates can fall out from the finished oil. The new molybdenum dithiocarbamate additives having superior short- and long-term solubility properties were developed [13].

According to [6], the occurrence of FMs can decrease engine fuel consumption by 2–4%.

As reported in [11], tribological tests were conducted using a pin-on-disc tribotester for steel/steel contact zones lubricated by different lubricants: 5W-30 engine oil, PAO and PAO + GMO (1% by weight of GMO). When lubricated with the API SG 5W-30 engine oil, friction of steel/steel combination was equal to 0.125. When GMO was used as additive in PAO, the steel/steel friction pair gave a friction coefficient of 0.1, and of 0.07 when the pure PAO was applied.

Sutton et al. [69] found that the addition of MoDTC to a standard additive package improved fuel economy by 0.4%, as did the addition of an organic FM.

Tseregounis et al. [73] during Sequence VIA and VIB tests, obtained a 2% fuel economy benefit by reducing oil viscosity from one of a SAE 10W-40 oil to that of a SAE 0W-10 oil using the same additives, and 2% from adding molybdenum FMs using the same base oil viscosity. Interesting results from engine tests were given in [42]. For an engine speed of 800 rpm, the total engine friction loss was higher for SAE 5W-30 oil with FM at low lubricant temperatures as compared with SAE 0W-20 oil without FM, but at oil inlet temperature of 80 °C the total frictional loss was nearly the same. The further increase in oil temperature could result in friction loss for SAE 0W-20 oil without FM exceeding this for SAE 5W-30 oil with FM. This was because of mixed to boundary friction loss becoming dominant at high oil temperature and under such conditions higher viscous oil reduced friction and the FM activated at higher temperatures, helped to reduce friction.

For engine speeds of 1500 rpm and 2000 rpm at lower oil inlet temperatures, the total engine friction for SAE 0W-20 oil without FM was lower than for SAE 5W-30 oil with FM. At higher temperatures the friction loss for SAE 0W-20 oil without FM exceeded that for SAE 5W-30 oil with FM.

For SAE 5W-30 oil with FM there could be a further decrease in friction loss with increase in oil inlet temperature as compared with that for SAE 0W-20 oil without FM.

The total engine friction loss for SAE 5W-30 oil with FM was about 12% higher than for SAE 0W-20 oil without FM as the former was more viscous, resulting in high shear loss. At oil inlet temperature equal to 80 °C, the total engine friction loss for SAE 0W-20 oil without FM was about 7% higher than that for SAE 5W-30 oil with FM. For any oil, at any engine speed, there was upward trend of the average friction with an increase in the bulk inlet temperature. An increase in the bulk inlet temperature led to a decrease in the oil viscosity and consequently a decrease of the oil film thickness which in turn caused an increase in the shear rate between the two mating surfaces. The increase in shear rate increased the friction between the two surfaces, but this effect was limited to a certain extent as the oil viscosity decreased at the same time. Also, the reduction of the film thickness resulted in more asperities coming into contact causing an increase in friction.

Many complicated interacting factors affected the friction process. Therefore, it is possible that under certain circumstances the increase in bulk inlet temperature can hardly affect increasing the friction and sometimes the reverse effect may result. Therefore, for the temperature range of 40–60 °C the increase in friction was small as compared with the range of 80–90 °C. For engine speed 1500 rpm, there was a slight decrease in friction for the oils SAE 10W-40 and SAE 5W-30 as the temperature increased from 40 to 60 °C. This was because at low temperatures the viscosity was high which under hydrodynamic lubrication conditions resulted in high shear losses, which then decreased as temperature increased causing a decrease in oil viscosity. But above 60 °C mixed to boundary lubrication became dominant and a rise in temperature caused an increase in friction.

The benefit of the FM present in the oils SAE 0W-20 and SAE 5W-30 was evident at high temperatures. At 40 °C the friction for the SAE 10W-40 oil was up to 3% higher than for the SAE 5W-30 oil in engine speed range between 800 and 2500 rpm. At 95 °C the friction for the SAE 10W-40 oil was up to 3% lower than for the SAE 5W-30 oil in engine speed range between 800 and 1100 rpm and up to 3% higher than for the SAE 5W-30 oil in engine speed range between 1100 and 2500 rpm. With increasing the engine speed, the friction force decreased faster at the temperature of 95 °C than at 40 °C.

The limiting coefficient of friction (μlim) for the SAE 0W-20 oil without FM was equal to 0.12 as compared with 0.08 for the oil with FM.

4.5 The Role of Anti-wear Additives

The most famous AW, the ZDDP, shows a superior performance as an anti-wear additive in engine oil [63, 81, 82]. It contains the combination of Zn, S and P producing protecting tribo-films. However, as ZDDP can poison the automotive catalyst used for emissions control, the amount of ZDDP allowed in engine oils is limited. Zinc in ZDDP contributes to the ash content of the oil hindering operation of diesel engine diagnostics systems.

Therefore, there is a growing interest in ashless anti-wear additives. The first group consists of aryl phosphates, aryl
thiophosphates, amine phosphates and alkyl thiophosphates. They contain P reacting with the metal surface to produce anti-wear tribo-films. These P-based AWs can be alternatives to ZDDP in engine oil formulations required where lower ash contents are needed. The second group consists of ashless dithiocarbamates, sulfurized olefins and fats, and oil soluble dimercaptothiadiazole derivatives. They contain S and are P-free and enhance the elastic properties of the tribo-films. These additives can supplement other anti-wear additives such as ZDDP or organo-molybdenum compounds.

The AWs in engine oil can result in occurrence of Zn, S and P containing chemical compound in the PM emission.

5 Lubricants with TiO2 Nanoparticles

Some studies related to the effect of addition of TiO2 nanoparticles into lubricating oil on its tribological features can be found in the literature.

Nabhan and Rashid [45] studied tribological behavior of two types of lubricant oils with dispersed different amounts of SiO2 and TiO2 nanoparticles. Experiments were carried out at different temperatures, 40 °C, 80 °C, and 100 °C. The concentrations of nano oxide additives used in the experiment were 0.5% and 1.0% wt. The lowest values of the friction coefficient and wear rate were achieved for mineral and semi synthetic lubricant oils with addition of 1.0% wt. of TiO2 at 80 °C and 100 °C, respectively.

Laad and Jatti [33] studied the tribological behavior of titanium oxide (TiO2) nanoparticles as additives in mineral based multi-grade engine oil. It was found that the addition of TiO2 nanoparticles into engine oil decreased the friction and wear rate and hence improved the lubricating properties of engine oil. It was also observed that TiO2 nanoparticles possessed good stability in the engine oil and improved its lubricating properties.

Jatti [26] during studies utilized the mineral based multi-grade engine oil containing titanium oxide nanoparticles of average size of 10–25 nm. The nanoparticles were added to the lubricating oil at different concentrations (0.5–2% wt.) on the weight basis. The required quantity of nanoparticles was mixed with the lubricating oil. A Film Stripping device and lathe machine (at highest rpm) was used for mixing the nanoparticle additives in the lubricating oil. The time of mixing was fixed at 30 min based on the experience of the authors in producing a stable suspension.

According to Zin et al. [83], the Strieber curves showed that no significant changes in coefficient of friction were detected in presence of TiO2 nanoparticles in the oil.

Peng et al. [51] investigated the TiO2 nanoparticles dispersed steadily in lubricating oil by surfactant. The TiO2 nanoparticles were prepared by sol–gel method. It was shown that the TiO2 nanoparticles were decomposed during the friction process to form harder nano-film on metal surface or diffuse into base metal.

During studies carried out by Suryawanshi and Pattiwar [68], the TiO2 nanoparticles were added to the lubricating oil at 0.5% wt., as such nanoparticles are synthetically steady. Hence, the chances of a reaction with base liquid and tribo-surfaces were very low. The TiO2 nanoparticles were spherical with size distribution in the average range of 30–50 nm. It was found that the oil additive can prevent the agglomeration of nanoparticles. The structure of TiO2 nanoparticles remained
unchanged. A stirrer was used for the mixing of TiO₂ nanoparticle in the base lubricating oil. The speed for the mixing was kept at 1500 rpm. The time of mixing was 30 min in order to obtain a stable suspension. The oleic acid was used as a surfactant that modulated the available surface energy of the particles so that the surface tension decreases, preventing the aggregation process.

Ilie and Covâlău [25] added a certain amount of prepared TiO₂ nanoparticles to the base oil. The mixture was exposed to direct ultrasound irradiation in ambient air for 10 min. Ultrasound irradiation was realized with a high-intensity ultrasonic probe immersed directly in the reaction solution. Then, the solution was accomplished in an ultrasonic cleaning bath in ambient air for 15 min. After the above two procedures, the appearance of the base oil with nanoparticles was of a semi-transparent suspension. It was heated and stirred at 120 °C for 30 min, followed by cooling and standing. Finally, the transparent stable lubricants containing 0.1, 0.2, 0.3, 0.4, 0.5 wt.% TiO₂ nanoparticles were obtained.

6 Modeling of Chain Transmission

Some models of chain transmissions were elaborated with different level of their complexity.

Novotny and Pištek [49] focused on simulation of dynamics of the timing chain drive with the use of a multibody system. A mass-produced four cylinder in-line engine with two camshafts and two valves per cylinder has been used as a computational model.

Rodriguez et al. [56] developed a model of roller chain and sprocket dynamics. Therein, each chain link was modeled as a rigid body with planar motion, with three degrees of freedom and connected to adjacent links by means of a springs and dampers. The kinematics of roller–sprocket contacts was modeled in full detail. Sprocket motions in the chain’s plane, resulting from torsional and bending torques of attached camshafts were also considered. One or two-sided guides could be treated as well as stationary, sliding or pivoting tensioners operated mechanically or hydraulically. The model also considered the contact kinematics between chain link rollers and guides or tensioners. The model considered the effects of the dynamics of the chain drive on valvetrain behavior.

According to [30], the timing chain drives simulation results are often presented as families of function graphs (data series). Previously, the analysis of those results was based on static 2D diagrams and animated 3D visualizations. They were suitable for the detailed analysis of a few simulation variants, but not for the comparison of many cases. A new approach to the analysis, based on coordinated linked views and advanced brushing features was proposed. The proposed method introduced a novel, so-called segmented curve view, which could display distributions in families of function graphs.

According to [41] the optimized chain and belt drives can have similar efficiency. While chain drives have higher efficiency than dry belt drives, chain drives and wet belt drives perform similarly. A common dry belt has a strength-to-width ratio, which is twice lower than one for a similar chain application. Adaptability, low dynamic cam oscillation, strength and best-in-class NVH (Noise, Vibration, and Harshness) performance can make chain drives the best solution for timing drives. With proven long-term field durability, chain drives offer compact packaging, optimized efficiency and robustness against dynamic instability.

Egorov et al. [17] proposed a method allowing evaluation of the efficiency of a chain drive with a high measuring frequency rate within a wide range of possible modes of operation as it used the angular acceleration and the acceleration time as controlled variables. The method used the loading rotary bodies attached to a driven shaft of a chain drive to create the rated force in a chain, eliminating a need for a loader. The method allowed determining the mechanical efficiency of chain transmissions without consideration of the losses in their bearing units. It was experimentally proved that the method allowed to evaluate the quality of lubricants in the course of operation of a chain transmission.

According to [72], most of the friction in a chain drive comes from the movement of the bushings, pins and rollers. Such friction is a combination of Coulomb friction and viscous damping dependent on the lubrication conditions. It was not included in the model presented in [72], but damping was introduced to obtain a stable solution.

Kozlov et al. [32] proposed a new approach to the evaluation of the quality of lubricants for chain transmissions, which was based on the relationship between the chain efficiency pulldown and the use of inappropriate lubricants. They used a method utilizing rotary bodies with the known moments of inertia. The method allowed the investigation of the mechanical losses in a chain as most of the damping also occurs at this side. The damping force is usually much smaller than the stretching force in the chain but is related to it. The damping force in the slack span was neglected, as the stretching force at the slack span was smaller than at the tight span. For simplicity, a viscous damping force was assumed, which was proportional to the relative velocity between the two end points at the tight side.

The damping force was obtained from Eq. (1).

\[ F_d = D_{\text{chain}} \cdot \left[ R_{1_p} \cdot \frac{d\varphi_p}{dt} \cdot \cos \left( \varphi_{1_p} - \theta_{m_p} \right) - R_{1_g} \cdot \frac{d\varphi_g}{dt} \cdot \cos \left( \varphi_{1_g} - \theta_{m_g} \right) \right] \]

The angle \( \varphi \) was used to describe the position of the sprocket (Fig. 1). The rotation coordinates to the first contacting tooth’s center-line on the sprocket were \( \varphi_p \) and
\( \varphi \) for driving and driven sprocket, respectively. To describe the position of a specific \( i \)th roller the angle \( \varphi_i \) was used. The angles between the \( y \) axis and the first roller of each sprocket were \( \varphi_{1,p} \) and \( \varphi_{1,g} \) for driving and driven sprocket, respectively. The angles \( \theta_{\text{in.p}} \) and \( \theta_{\text{in.g}} \) were the chain angles, relative to the \( x \) axis, of the first links in contact with the driving and driven sprocket, respectively.

7 The PM Emission in the SI Engine

Problem of the PM emission is important both in CI and SI engines due to severe restrictions (below 0.005 g/km) introduced by the standards such as EURO5 or EURO6.

According to [37], the nanoparticle emissions from SI engines can differ considerably, both for newer engines and for older ones, but they are comparable to typical Diesel engine emissions. This investigation mainly focuses on the metal oxide particles. Very clearly, metal oxides are being emitted in the size range \( 10–30 \) nm. The ash particle concentration mostly exceeds the soot particle concentration and can even exceed the ash emission from the Diesel engines. The SI engines also emit very high concentration of solid particles in the critical size range smaller than 200 nm. The emission of ash particles can reach a non-negligible level. The true toxic substances can be the elemental carbon of soot, the organic deposits on the soot particles, the attached metal oxide particles, or their combination.

Although in the current tests no exhaust gas analysis was carried out for the model engine lubricated with oil without and with a 2\% wt. TiO\(_2\) nanoparticles, such studies are foreseen during further tests. The tested, relatively not recent, engine did not possess a particle catalyst. The latter is necessary in spark-ignition engines to ensure compliance with stringent exhaust emission standards, i.e., EURO5 or EURO6.

The detailed measurement of metallic nanoparticle emission is difficult and expensive. For example, according to [75], online particle analysis can be performed with the Scanning Mobility Particle Sizer (SMPS). Size fractionated chemical analysis of nanoparticles in vehicle emissions were carried out by sampling with an electrical low-pressure multi-stage impactor ELPI with subsequent acid digestion in a microwave system and chemical analysis with plasma mass spectrometry ICPMS.

Giechaskiel et al. [20] described the instrumentation like gravimetric filter measurement, used for the particulate emission measurement. In addition, other popular methods and instruments were analyzed, like chemical analysis of filters, light extinction, scattering and absorption instruments, electrical mobility, and particle counting instruments.

The mechanisms of solid particles formation in the SI engines are different and complex.

According to [55], PM emissions from Gasoline Direct Injection (GDI) engines are complex mixtures of volatile and non-volatile materials containing soot, organic carbon and hydrocarbons. GDI-derived particles are composed of nucleation mode (< 50 nm) and accumulation mode (50–200 nm).

Nucleation mode particles are usually organic carbons (VOCs) originated, i.e., from an engine oil, but can be also solid particles as well. Accumulation mode particles comprise carbonaceous soot particles with an elemental carbon structure and adsorbed volatile material.

Volatile particles including sulfates, nitrates, and organic carbon (OC) can be generated by partial combustion of the engine oil and present in the form of vapor or liquid phase particles in GDI engine exhaust.

Sonntag et al. [62] explained that engine oil coats the piston and cylinder walls, from which semi-volatile organic compounds (SVOC) desorb during the exhaust stroke, providing a major pathway for oil consumption and PM emissions.

Engine oil is continually consumed in the combustion chamber by about 0.2\% [27] or as low as 0.1\% in modern engines [2], but sometimes, it also contributes in particulate matter formation [16, 53]. Sonntag et al. [32] stated that the engine oil contributes to PM emissions from gasoline engine by about 25\%. For modern turbocharged GDI engines Pirjola et al. [53] found that the PM emissions during transient operation strongly depend on the engine oil, and a 78\% reduction in PN emissions was obtained solely by changing its properties. The concentration of additives (Zn, Mg, P and S) in engine oil positively correlate with PN emission and the engine oils containing high metal (Zn, Ca, Mg) and S content contributed in higher PM emissions.

According to [23], absorption of fuel vapor into oil layers on the cylinder wall during intake and compression strokes followed by desorption of fuel vapor during expansion and exhaust strokes results in formation of organic carbon (OC) particles, which often are volatile.
Metallic particles including Fe, Cu, Ni or other metallic compounds as well as metallic oxides, are found in engine exhaust which originate from engine oil, wear of engine parts, and engine oil additives containing metal organic elements. Engine oil transfers these particles into combustion chamber where they partially vaporize and form extremely fine particles (less than 50 nm) [37].

8 The Effect of Occurrence of TiO$_2$ Nanoparticles in Engine Oil on the Engine Emission

The effect of the occurrence of TiO$_2$ nanoparticles in engine oil on engine emissions can be manifested in two ways:

- By changing the total engine friction, particularly one in the timing chain transmission, what causes a change in the engine operating point for given load conditions and fixed values of other parameters affecting engine operation,
- By changing the composition of the exhaust gases, caused, i.e., by burning engine oil containing TiO$_2$ entering the combustion chambers.

8.1 The Oil Consumption Affecting the PM Emission in the Analyzed Engine—Calculation Example

Although there were no data according the oil consumption in the investigated engine, it can be estimated based on the data obtained for similar SI engines. For the petrol engines utilized in Toyota Corolla VVTI 1.4 99 KM and Toyota Corolla VVTI 1.6 109 KM such a consumption was equal to 1 L/1000 miles. For Toyota Avensis it can reach 2 L/1000 miles or even 5 L/1000 miles. For Toyota 4E-FE 1.3 L 55 kW straight-four 4-stroke natural aspirated gasoline engine the engine oil consumption was also equal to 1 L/1000 miles. For the further calculations, it was assumed that the average vehicle speed was equal to 60 mil/h, which corresponded to 1.6 km/min. This resulted in driving time equal to 1000 min.

It was also assumed that the average engine speed was equal to 3000 rpm. It resulted in 1,500,000 rotations of the engine crankshaft. The engine oil consumption was equal to 6.7·10$^{-7}$ L/cycle. The density of SAE 10W-40 oil was equal to 900 kg/m$^3$. When such an engine oil contains 2% wt. of TiO$_2$ nanoparticles, the emission is equal to 1.227·10$^{-8}$ g TiO$_2$/cycle and to 0.000012 g of TiO$_2$/km.

When the progressive wear of the engine is considered, its oil consumption increases five times and the TiO$_2$ nanoparticles emission can reach even up to 0.00006 g/km.

9 Materials and Methods

9.1 Model of the Analyzed Chain Transmission

The analyzed chain transmission was from the SI combustion engine Toyota Corolla 1.4 VVTI (Fig. 2).

In the present study the model contained three assemblies:

1. Assembly of the crankshaft with its sprocket and its flywheel,
2. Assembly of the outlet camshaft with its sprocket,
3. Assembly of the inlet camshaft with the phaser and its sprocket, elaborated with the finite element method.

The mentioned assemblies were connected through the one row chain 4.

The camshaft and crankshaft assemblies were treated as stiff solid bodies connected with bearings through contact elements. The crankshaft assembly rotated with constant rotational speed usually equal 120 rpm but for one case the full chain assembly rotated also with an assumed lower speed of 60 rpm. The chain was modeled as the set of solid rigid components connected by contact elements. The model components enabled determination of their weights and mass inertia moments.

![Fig. 2 The chain transmission components](image)

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[37]: Reference number 37, which is not visible in the image, should be added according to the source of the material.
9.2 Experimental Stand for Friction Studies in the Chain Transmission

The friction in the chain transmission was determined using the stand equipped with the original SI engine with some modifications. The crankshaft assembly was supported in two border mean journal bearings of crankshaft, in which the original bronze half-shells were replaced by ones made of PTFE. This was to reduce the friction coefficient between the crankshaft journals and their half-shells.

The outlet and inlet camshaft assemblies were supported in their border pairs of journal bearings. To decrease the friction coefficient, in the bushing covers of the bearings the threaded holes were made to place grease nipples supplying lithium grease into the contact zones between camshaft journals and their bushings. The grease was continuously replenished in the bearings using a grease gun.

The self-starter driving flywheel connected with the camshaft was placed in the engine body through the set of screws, which was a little different than in the original vehicle. The self-starter was supplied with voltage from the battery. In the original construction the chain was tensioned by the tensioning piston supplied with the oil pressure and acting on swingable guide. However, in the stand the piston with the top plane was replaced by the piston with a roller. The position of the latter can be changed manually. This allows a quick disconnection of the front piston plane from the pressing guide.

9.3 The Determination of Total Friction Torque in the Chain Transmission

The total friction torque in chain transmission was determined in several steps.

The subassembly was arranged in such a way that the crankshaft related to the flywheel and the sprocket. Its mass inertia moment was equal to \( I \). The crankshaft subassembly was driven by the self-starter to the predetermined rotational speed of 120 rpm and then braked by the friction torque \( M_{T1} \) occurring in two crankshaft main bearings up to stop. The time \( t_1 \) of breaking the whole system was registered.

Next, the outlet camshaft subassembly sprocket was driven by special device containing the drive unit (modified drill), three-jaw lathe chuck and the disconnect-able friction clutch. When the outlet camshaft subassembly reached the rotational speed of 120 rpm the clutch was disconnected by the auxiliary servo-valve after supplying the control electrical signal to its coil. The mass inertia moment of the outlet camshaft assembly with its sprocket was equal to \( I_2 \). The outlet camshaft subassembly was braked by the friction torque \( M_{T2} \) occurring in its two bearings up to stop. The time \( t_2 \) of braking of the assembly was registered.

Next, the procedure was repeated for the inlet camshaft assembly containing the phaser and the sprocket. The mass inertia moment was equal \( I_3 \). The time \( t_3 \) of breaking the assembly by the friction torque \( M_{T3} \) occurring in its two bearings was registered.

Then the angular decelerations \( \varepsilon_1, \varepsilon_2, \varepsilon_3, \varepsilon_4, \varepsilon_5 \) were obtained from Eqs. (2)–(4), and the inertia moments were determined from Eqs. (5)–(7).

\[
\begin{align*}
\varepsilon_1 &= \omega_0/t_1 \\
\varepsilon_2 &= \omega_0/t_2 \\
\varepsilon_3 &= \omega_0/t_3 \\
M_{T1} &= I_1 \cdot \varepsilon_1 \\
M_{T2} &= I_2 \cdot \varepsilon_2 \\
M_{T3} &= I_3 \cdot \varepsilon_3 
\end{align*}
\]

Finally, the self-starter drove up to the predetermined crankshaft rotational speed the full assembly. The full assembly contained three subassemblies. The first was the crankshaft with flywheel and sprocket. The second was the inlet camshaft with original phaser and sprocket. The third was the outlet camshaft with the original sprocket. All subassemblies were connected through the original chain mating with its guides and tensioned by the modified tensioner piston. Then, self-starter was turned off and the full assembly was braked up to stop by the friction torques: \( M_{T1} \) in two crankshaft bearings, \( M_{T2} \) in two outlet camshaft bearings, \( M_{T3} \) in two inlet camshaft bearings, respectively and \( M_{int1}, M_{int2} \) and \( M_{int3} \) friction torques occurred in three groups of segments of the chain transmissions (Fig. 3). The time \( t_4 \) of breaking the chain assembly was registered. The angular deceleration \( \varepsilon_4 \) was obtained from Eq. (8).

\[
\varepsilon_4 = \omega_0/t_4
\]
The internal friction torque $M_{\text{int}}$ in the chain transmission was estimated using the scheme in the Fig. 1 and Eqs. (15)–(26). It was assumed that such torque contains three components:

\[
\begin{align*}
M_{\text{int}} &= M_{\text{int}0} + M_{\text{int}1} + M_{\text{int}2} + M_{\text{int}3} \\
M_{\text{int}1} &= M_{\text{T1c}} + M_{\text{T21c}} + M_{\text{T3c}} \\
M_{\text{int}2} &= M_{\text{r1}} + M_{\text{T1}} + M_{\text{T21}} + M_{\text{T3}} \\
M_{\text{int}3} &= M_{\text{T1}} + M_{\text{T21}} + M_{\text{T3}}
\end{align*}
\]

9.4 The Determination of the Friction Torque Between Chain Components

The friction torque occurring between the chain roller and the pin was estimated experimentally. The friction between the neighboring chain segments (outer and inner one) in each pair

\[
\begin{align*}
M_{\text{int}} &= \text{related to the chain resistance to motion occurring in the crankshaft sprocket vicinity,} \\
M_{\text{int2}} &= \text{related to the chain resistance to motion occurring in the outlet camshaft sprocket vicinity,} \\
M_{\text{int3}} &= \text{related to the chain resistance to motion occurring in the inlet camshaft sprocket vicinity.}
\end{align*}
\]

It was also assumed that such components are equal to $M_{\text{int0}}$. The friction torques in the crankshaft bearing $M_{\text{T1c}}$, in the outlet camshafts bearing $M_{\text{T21c}}$, and in the inlet camshaft bearing $M_{\text{T3c}}$ during breaking of the studied full chain transmission assembly can be estimated from Eq. (28). In Eq. (29), $r$ was the pitch radius for the crankshaft sprocket and $R$ was the pitch radius for the inlet camshaft sprocket and for the outlet camshaft sprocket.

\[
\begin{align*}
(N_1-N_3) \cdot r &= M_{\text{T1c}} + I_1 \cdot \varepsilon_6 + M_{\text{int1}} \\
(N_2-N_1) \cdot R &= M_{\text{T21c}} + (I_2 + I_{21}) \cdot (\varepsilon_6/2) + M_{\text{int2}} \\
(N_3-N_2) \cdot R &= M_{\text{T3c}} + I_3 \cdot (\varepsilon_6/2) + M_{\text{int3}} \\
M_{\text{T1c}} &= M_{\text{T1}} + M_{\text{T21c}} + M_{\text{T3c}} = M_{\text{T3}} \\
M_{\text{T1}} &+ M_{\text{T21}} + M_{\text{T3}} + I_3 \cdot \varepsilon_6/2 + M_{\text{int2}} + M_{\text{T3c}} + I_3 \cdot \varepsilon_6/2 + M_{\text{int3}} \\
&+ (I_2 + I_{21}) \cdot \varepsilon_6/2 + M_{\text{int3}} + I_3 \cdot \varepsilon_6/2 + M_{\text{int3}} \\
&= 0 \\
R/r &= 2 \\
M_{\text{int}} &= M_{\text{int0}} + M_{\text{int2}} + M_{\text{int3}} \\
M_{\text{int1}} &= M_{\text{int2}} + M_{\text{int3}} = M_{\text{int0}} \\
M_{\text{int}} &= 3 \cdot M_{\text{int0}} \\
2 \cdot M_{\text{T1c}} + 2 \cdot I_1 \cdot \varepsilon_6 + 2 \cdot M_{\text{int1}} + M_{\text{T21c}} + (I_2 + I_{21}) \cdot \varepsilon_6/2 + M_{\text{int2}} + M_{\text{T3c}} + I_3 \cdot \varepsilon_6/2 + M_{\text{int3}} \\
&= 0 \\
2 \cdot M_{\text{T1c}} + 2 \cdot I_1 \cdot \varepsilon_6 + (4/3) \cdot M_{\text{int}} + M_{\text{T21c}} \\
&+ (I_2 + I_{21}) \cdot \varepsilon_6/2 + M_{\text{T3c}} + I_3 \cdot \varepsilon_6/2 \\
&= 0 \\
M_{\text{int}} &= -(3/4) \cdot [2 \cdot M_{\text{T1c}} + M_{\text{T21c}} + M_{\text{T3c}} + 2 \cdot I_1 \cdot \varepsilon_6 + (I_2 + I_{21} + I_3) \cdot \varepsilon_6/2] = 0
\end{align*}
\]
was neglected. It was assumed that two rollers with two inner segments create one rigid body and two pins with two outer segments create the other rigid body. The friction torque was measured using the concept of the physical pendulum.

Before the measurement the chain was placed in the ultrasonic bath for the 3 min to remove the residual particles of lubricant existing in the contact zones between the rollers and pins of the chain.

Then one chain pin was fixed using a small vice. Then, the chain segments swung relative to the axis of the fixed roller. To make the set of chain segments close to one rigid body, the friction torque was neglected. It was assumed that two rollers with two inner segments create one rigid body and two pins with two outer segments create the other rigid body. The friction torque was estimated from Eq. (29). According to Eq. (1), the friction between chain components is related to the speed of their motion. The internal friction torque \( M_{\text{int}} \) in the chain transmission is also related to the friction torque \( M \) between the chain rollers and pins. During operation the estimated number \( k \) of chain rolls clearly sliding against mating pins was obtained from Eq. (30).

\[
k = \pi \cdot (r + 2 \cdot R)/p
\]

where \( p \) — chain pitch.

It was assumed that the dry internal torque \( M_{\text{int}} (M_{\text{rdry}}, \omega_1) \) in the chain transmission is related to the dry friction torque \( M_{\text{rdry}} \) between the chain roller and the pin. It is also related to the constant value of rotational speed \( \omega_1 \) of the crankshaft. This is described by Eq. (31). The dry friction torque \( M_{\text{rdry}} \) is obtained using physical pendulum method according to Eq. (31).

\[
M_{\text{int}} (M_{\text{rdry}}, \omega_1) = A \cdot k \cdot M_{\text{rdry}} + B \cdot \omega_1
\]

Next, it was considered the case when the chain transmission and so each contact zone between the chain roller and the pin was lubricated by the engine oil 10W-40. Similarly, the internal friction torque \( M_{\text{int}}(M_{\text{rol}}, \omega_1) \) in the chain transmission is related to the friction torque \( M_{\text{rol}} \) in contact zone between the chain roller and the pin. It is also related to the constant value of rotational speed \( \omega_1 \) of the crankshaft. This is described by Eq. (32). The friction torque \( M_{\text{rol}} \) in contact zone between the chain roller and the pin lubricated with the oil 10W-40 was obtained using the mentioned physical pendulum method.

\[
M_{\text{int}} (M_{\text{rol}}, \omega_1) = A \cdot k \cdot M_{\text{rol}} + B \cdot \omega_1
\]

Then, the case when the chain transmission and so each contact zone between the chain roller and the pin was lubricated by the engine oil 10W-40 with 2 wt.% amount of TiO\(_2\) nanoparticles was studied. Also, in this case, the internal friction torque \( M_{\text{int}}(M_{\text{TiO}_2}, \omega_1) \) in the chain transmission is related to the friction torque \( M_{\text{TiO}_2} \) in contact zone between the chain roller and the pin. It is also related to the constant value of rotational speed \( \omega_1 \) of the crankshaft. This is described by Eq. (33). The friction torque \( M_{\text{TiO}_2} \) in contact zone between the chain roller and the pin lubricated with the oil 10W-40 with 2 wt.% amount of TiO\(_2\) nanoparticles was obtained using the mentioned physical pendulum method.

\[
M_{\text{int}} (M_{\text{TiO}_2}, \omega_1) = A \cdot k \cdot M_{\text{TiO}_2} + B \cdot \omega_1
\]

For two values of crankshaft rotational speed, namely \( \omega_1 = 0.12 \) rad/s and \( \omega_1 = 0.06 \) rad/s, two different values of the dry internal torque \( M_{\text{int}}(M_{\text{rdry}}, \omega_1) \) were determined from Eq. (31) and then the constants \( A \) and \( B \) were estimated.
9.5 Preparation of the Analyzed Mixture of Engine Oil with TiO₂ Nanoparticles

Based on information obtained from [25, 26, 33, 45, 51, 68, 83], a mixture of the engine oil with dispersed 2% wt. of TiO₂ nanoparticles was prepared. When such a relatively high amount of TiO₂ nanoparticles is added to the analyzed engine oil, there is a potential risk that the resulting system creates unstable dispersion. Therefore, an addition of acid oil was needed to stabilize the nanoparticles. When the lube system is not stable, the decrease of friction resistance is more likely due to the formation of the thin TiO₂ coating on metallic hardware contacts rather than the stable composition of lubricating fluid. However, the phenomenon of nanoparticles agglomeration is inevitable. It results in generation of relatively big particles, which can be absorbed in the oil filter, so the amount of TiO₂ in real engine oil can be lower.

A volume of 1 L of commercial engine oil SAE 10W-40 was weighed to obtain 0.9 kg. A sample of 18 g TiO₂ nanoparticles of average size of 20 nm (as delivered) was weighed using a precision balance. Such an amount of TiO₂ nanoparticles was added to the engine oil. A stirrer was used for the mixing of TiO₂ nanoparticle in the engine oil. The speed for the mixing was kept at 1500 rpm. The time of mixing was 30 min in order to obtain a stable suspension. The volume of 10 cm³ of oleic acid was used as a surfactant modulating the surface energy of the particles so that the surface tension decreases. This allowed partial, however not complete, limitation of the aggregation process of the TiO₂ nanoparticles.

9.6 Modeling the Friction Coefficient in Contact Lubricated by Engine Oil

The resulting relation (the ratios of values obtained for the friction torques) between friction resistance in steel/steel contact zones unlubricated, lubricated by the reference pure synthetic SAE10W-40 engine oil and by this oil with the 2% wt. amount of TiO₂ nanoparticles can be used with the highest confidence level in other steel/steel contact zones lubricated under the same or very close conditions. In order to allow extrapolation of such a relation for the other oils, the assumed formulas are utilized. The closer are features of the other oil to these of the reference one, the more valuable are extrapolated results.

Srník and Pfeiffer [65] proposed that without significant loss of accuracy, the friction coefficient between the bolt of the chain link and the pulley can be approximated by a smooth nonlinear function.

According to [47], a model of the coefficient of friction which considers the dynamics associated with kinetic friction, and the dynamics associated with stiction and Striebeck effects (which are prominent under dry and lubricated contact conditions, respectively) can be used. The present study assumed the same model, given by Eq. (34).

\[
\mu = \mu_0 \left(1 - e^{\kappa v_{rel}}\right) \left(1 + \left(\sigma - 1\right)e^{-\chi v_{rel}}\right)
\]

(34)

where:
- \( \mu \) — coefficient of friction between link and pulley
- \( \mu_0 \) — coefficient of friction between link and pulley
- \( v_{rel} \) — relative velocity between contacting surfaces.

The speed \( v_{\text{min}} \) corresponding to the minimum friction coefficient was determined based on the Hersey number \( H_e_{\text{min}} \) related to \( v_{\text{min}} \) and results presented in [31]. It is good to remind here the commonly known definition of the Hersey number, namely \( H_e = \frac{\eta v_{\text{min}}}{P/l} \), where:
- \( \eta \) — dynamic viscosity of oil lubricating contact zone
- \( v_{\text{slip}} \) — slip speed of mating surfaces
- \( P/l \) — unit force loading contact zone (\( P \) — loading force; \( l \) — the length of contact in direction perpendicular to the slip direction of the bodies).

Kovalchenko et al. [31] studied friction in contact zone between polished steel surfaces lubricated by two PAO-based oils (Mobil-1). The studies were carried out with a pin-on-disk apparatus at sliding speeds in the range of 0.015–0.75 m/s and nominal contact pressures that ranged from 0.16 to 1.6 MPa.

The first oil showed density of 852 kg/m³ and viscosities 54.8 cSt at 40 °C and 10.1 cSt at 100 °C the Hersey number \( H_{e_{\text{min}}} \) corresponding to the minimum friction coefficient was equal to 0.82 \( \frac{\text{cSt} \cdot \text{s}}{\text{N} \cdot \text{m}^3} \). 852 kg/m³ · 4.7 mm = 0.00000328. The second oil showed density of 863 kg/m³ and viscosities 124.7 cSt at 40 °C and 17.7 cSt at 100 °C and the Hersey number equal to 0.78 \( \frac{\text{cSt} \cdot \text{s}}{\text{N} \cdot \text{m}^3} \). 863 kg/m³ · 4.7 mm = 0.00000316.

Assuming that the Hersey number \( H_{e_{\text{min}}} \) corresponding to the minimum friction coefficient depends linearly only on the dynamic velocity \( \eta(T) \) it can be estimated from Eq. (35).

\[
H_{e_{\text{min}}} (\eta) = \frac{H_{e_{\text{min}}} (\eta = 124.7 \text{ cSt}) - H_{e_{\text{min}}} (\eta = 54.8 \text{ cSt})}{124.7 \text{ cSt} - 54.8 \text{ cSt}} \cdot \eta(T)
\]

(35)

\[
= -1.7 \cdot 10^{-9} \left[ \frac{1}{\text{cSt}} \right] \cdot \eta(T) + 3.4 \cdot 10^{-9}
\]

Such a relationship reflects well the value of \( H_{e_{\text{min}}} (\eta) \) published in [60] for PAO oils with different viscosities.
During analysis described in [64] the following values were used: \( \mu_0 = 0.25, \sigma = 3.5, \kappa = 10, \chi = 3 \).

The same equation and its parameters were assumed for the modeled friction coefficient in the further analysis.

The parameter \( \chi \) strictly depends on dynamic viscosity \( \eta \) of lubricating oil.

It could be assumed that this dependency is given by Eq. (36).

\[
\chi \left( T_{\text{ref}}, VI_{\text{ref}}, \text{SAEclass}_{\text{ref}}, \text{APIgroup}_{\text{ref}}, \varepsilon_{\text{ref}} \right) \approx \frac{\eta \left( T, VI, \text{SAEclass}, \text{APIgroup}, \varepsilon \right)}{\eta \left( T_{\text{ref}}, VI_{\text{ref}}, \text{SAEclass}_{\text{ref}}, \text{APIgroup}_{\text{ref}}, \varepsilon_{\text{ref}} \right)}
\]

where:

\( T \) — considered temperature of oil
\( T_{\text{ref}} = 293 \) K — reference temperature of oil
\( VI \) — Viscosity Index of a considered oil
\( VI_{\text{ref}} = 163 \) — Viscosity Index of the reference oil
\( \text{SAEclass}_{\text{ref}} = 10W-40 \) — SAE class of the reference oil
\( \text{APIgroup}_{\text{ref}} \) — API group of the reference oil
\( \varepsilon \) — the amount of nanoparticles in a considered oil
\( \varepsilon_{\text{ref}} = 0 \) — amount of nanoparticles dispersed in reference oil

For the case of unlubricated contact zone \( \chi = \infty \).

### 9.7 Consideration on the Simultaneous Effect of the Temperature and Aging of the Engine Oil on Its Viscosity

According to [46], the variation of dynamic viscosity of the fresh SAE 10W-40 engine synthetic oil as a function of temperature can be estimated from Eq. (37).

\[
\eta(T) = 1.455 \cdot \exp(-0.06875 \cdot T) + 0.00421 \cdot \exp(0.024975 \cdot T)
\]

(37)

For the aged SAE 10W-40 engine synthetic oil the analytical equation has a form (38).

\[
\eta(T) = 0.75 \cdot \exp(-0.050785 \cdot T) + 5.008 \cdot 10^{-17} \cdot \exp(0.43185 \cdot T)
\]

(38)

The variation of the dynamic viscosity for the engine oil SAE10W40 is more than 19% at 25 °C and more than 28.5% at 75 °C.

### 9.8 Consideration on the Simultaneous Effect of API Group and the Oil Aging on the Oil Film Thickness

The largest share in engine friction is friction in the piston-ring-cylinder assembly, so the most important role plays the minimal thickness \( h \) of engine oil film in zones between them. It depends on the phase angle of crankshaft as reported in [46] or in [61].

According to [46], the minimum film thickness has insignificant variation through the crankshaft angles for the fresh and aged SAE10W40 oil at 40 °C, whereas very high variation appears as temperature increases. In practical terms, there is a significant reduction in the order of 13.5%, for example in 300 degrees, due to the lubricant’s viscosity temperature variations for 2 MPa test pressure at 75 °C.

The variation of the total piston ring friction is almost 7.8% at the TDC between fresh and aged oil.

The smaller value concerns aged oil, due to its slight viscosity variations at 40 °C. Instead, boundary friction is higher, 19.25% at 75 °C, for aged oil than for fresh oil. The aged oil significantly influences in engine friction losses.

According to [12], the friction coefficient varies with the thickness of engine oil film in contact zone, according Eqs. (39)–(41).

For engine oil from API IV group.

\[
\mu(h) = -0.025 \cdot \arctg(1.25 \cdot \pi \cdot \log_{10} h - \pi) + 0.042
\]

(39)

For engine oil from API III group.

\[
\mu(h) = -0.023 \cdot \arctg(1.2 \cdot \pi \cdot \log_{10} h - 1.005 \cdot \pi) + 0.045
\]

(40)

For engine oil from API II group.

\[
\mu(h) = -0.021 \cdot \arctg(1.15 \cdot \pi \cdot \log_{10} h - 1.01 \cdot \pi) + 0.048
\]

(41)

### 9.9 The Effect of the Content of Additives in the Engine Oil on the Modeled Friction Coefficient

According to [67], the mechanical friction losses can account for up to 9% of total SI engine losses.

It was assumed in the model that use of engine oil containing amount of friction modifiers or other additives different than the one in reference, the 10W-40 oil can result in obtaining friction coefficient differing by up to 2.5% relative to the case of reference oil. It is described by Eq. (42).

\[
\mu_{\text{oil}} = \mu_{\text{SAE10W-40}} \pm 0.025 \cdot \mu_{\text{SAE10W-40}} \cdot \frac{\varepsilon_{\text{FMoil}} - \varepsilon_{\text{FMSAE10W-40}}}{\varepsilon_{\text{FMoil}}}
\]

(42)

where:

\( \mu_{\text{oil}} \) — friction coefficient for analyzed oil
\( \varepsilon_{\text{FMoil}} \) — amount of FMs or other additives in relation to total weight of the analyzed oil
\( \mu_{SAE10W-40} \) — friction coefficient for reference SAE 10W-40 synthetic oil

\( \varepsilon_{FMSAE10W-40} \) — amount of FMs or other additives in relation to total weight of reference SAE 10W-40 synthetic oil

For example, the amounts of additives (wt.%) in engine oil are the following [18]:

For SAE 10W-40: Ca 0.43, Mg 0.004, Na 0.005, P 0.12, S 0.32, Zn 0.135

For SAE 10W-30: Ca 0.396, Cl 0.009, N 0.098, P 0.121, S 0.55, Zn 0.132

### 9.10 Determination of Changes in Engine Emissions

The estimation of emission changes needs the characteristics of the SI engine used for calculation of the friction torque in the chain transmission. Such characteristics were shown in Fig. 5.

The estimation of changes in emission of the analyzed engine caused by addition, through dispersion, of 2% TiO\(_2\) nanoparticles into lubricating oil was as follows.

As was mentioned, according to [3], the timing drive and valve train generate approx. 20% of overall engine friction losses depending on the engine speed.

According to [28] the total engine friction power contains five main components with following contributions to it, namely, crankshaft friction 9%, reciprocating friction 36%, valvetrain friction 16%, so called accessories friction 13%, and pumping losses 27%. In the model used during investigations, the so-called accessories friction and pumping losses were independent on the oil viscosity.

In the present analysis it was also assumed that the so-called accessories friction and pumping losses are almost independent on the addition of TiO\(_2\) nanoparticles into oil.

It was also assumed that addition of 2% of TiO\(_2\) nanoparticles into oil resulted in decreasing the friction losses in all bearings and piston groups by 10%.

So, addition of TiO\(_2\) nanoparticles into oil reduces total friction losses by 7–7.7%. Additionally, it causes that the timing drive and valve train generate about 14.4–18% of the overall engine friction losses.

Engine characteristics P(n) for the full load (θ = 0) before and after addition of 2% TiO\(_2\) nanoparticles into engine oil were calculated using two formulas:

\[
P(n, \theta = 1, \text{oil} + 2\% \text{nano TiO}_2) = P(n, \theta = 1, \text{pure oil}) + 0.07 \cdot P_T(n, \theta = 1, \text{pure oil})
\]

\[
P(n, \theta = 0, \text{oil} + 2\% \text{nano TiO}_2) = P(n, \theta = 0, \text{pure oil}) + 0.077 \cdot P_{\text{max}}(n, \theta = 1, \text{pure oil})
\] (44)

The data from [28] allowed calculation the ratios of total engine friction power losses \( P_T \) to maximal engine power \( P_{\text{max}} \) as a function of engine speed. The ratios were obtained for different values of engine load. Such characteristics were presented in Fig. 6.

Obtained characteristics for pure oil and for oil with addition of 2% TiO\(_2\) nanoparticles is shown in the Fig. 7.

Table 2 contains the throttle opening for different engine speed.

It was assumed that for the given engine speed related changes of its emissions, namely, \( \Delta \text{CO}, \Delta \text{CO}_2, \Delta \text{HC}, \Delta \text{NO} \) and \( \Delta \text{NO}_x \) can be calculated. They are proportional to
the throttle angle change $\Delta \theta$, engine torque change $\Delta M$, fuel consumption change $\Delta g$ and engine power $P$.

It was assumed that such proportionality is described by Eqs. (45)–(51).

$$\frac{\Delta CO(n, P)}{CO_{max}(P)} = k_{CO} \sqrt[4]{\frac{\Delta \theta}{\theta_{max}} \cdot \frac{\Delta M(n, \Delta \theta)}{M_{max}} \cdot \frac{\Delta g(n, \Delta \theta)}{g_{min}} \cdot \frac{P}{P_{reference}}}$$  

(45)

$$\frac{\Delta CO_2(n, P)}{CO_{2max}(P)} = k_{CO_2} \sqrt[4]{\frac{\Delta \theta}{\theta_{max}} \cdot \frac{\Delta M(n, \Delta \theta)}{M_{max}} \cdot \frac{\Delta g(n, \Delta \theta)}{g_{min}} \cdot \frac{P}{P_{reference}}}$$  

(46)

$$\frac{\Delta NO(n, P)}{NO_{max}(P)} = k_{NO} \sqrt[4]{\frac{\Delta \theta}{\theta_{max}} \cdot \frac{\Delta M(n, \Delta \theta)}{M_{max}} \cdot \frac{\Delta g(n, \Delta \theta)}{g_{min}} \cdot \frac{P}{P_{reference}}}$$  

(47)

$$\frac{\Delta NO_x(n, P)}{NO_{x, max}(P)} = k_{NO_x} \sqrt[4]{\frac{\Delta \theta}{\theta_{max}} \cdot \frac{\Delta M(n, \Delta \theta)}{M_{max}} \cdot \frac{\Delta g(n, \Delta \theta)}{g_{min}} \cdot \frac{P}{P_{reference}}}$$  

(48)

For the further analysis, the data related to the combustion engine presented in [1] were used. It was assumed that $P_{reference} = 68$ kW, $M_{max} = 111$ Nm, $g_{min} = 50$ g kW$^{-1}$ h$^{-1}$.

For that engine and for the assumed ratios $\Delta \theta/\theta_{max} = 0.5$ and $P/P_{reference} = 1$ it was estimated that $k_{CO} = 0.1434$, $k_{CO_2} = 0.069$, $k_{NO} = 0.1297$, $k_{NO_x} = 0.1204$, $k_{HC} = 0.1191$. These factors were slope factors of the linear regression lines presented in Fig. 8.

### 9.11 Methods for Measurement of PM Emission

Authors decided to modernize the exhaust system (Fig. 9) for the gasoline particulate filter (GPF) installation. The Exhaust Manifold 1 is not changed, but the Front Pipe 2 is adapted to the inlet of the GPF 3. The GPF is used in a modern SI engine with a similar design and power configuration. The GPF 3 is removable, in order to allow measuring PM emissions in exhaust gases (GPF removed) or assessing the effect of the GPF on exhaust gas flow (GPF fitted). This requires interfering in the exhaust system in order to mount the GPF in series with an existing Catalytic Converter 4 and Central Silencer 5. The Muffler 6 of exhaust system is not changed, but the tail pipe connecting the Muffler 6 with the Blower 11 relates to additional inlet and outlet pipe connected to Diluting Canal 8.

The exhaust gases flow partially through the tail pipe directly to the Blower 11 and partially through the Diluting Canal 8. The filter samples placed in the P-Filter 9 (Particulate Filter) both these remaining clean during flow of air and these containing deposited particles during flow of diluted exhaust gases were collected and weighted using the microbalance. The differences in such weights allow estimation of the mass emission of solid particles, as described in [5]. The mass composition of the samples is determined using chromatographic analysis and thus the amount of TiO$_2$ nanoparticles in the exhaust gas can be estimated. The air supplied to the Diluting Canal 8 is conditioned not in the climatized chamber, as described in [75], but using the elaborated Air Conditioner 7. The stream 10 of air is forced by a screw compressor cooperating with the system of bleeding valves. The stream 10 is directed to the chamber of the Air Conditioner system 7. The system 7 contains the electrical
heater, the heat exchanger transferring the heat from the chamber to the external heat radiators system. This system is cooled by a stream of air forced by a fan. In addition, a humidifier and air dryer are mounted in the chamber. Both the heater, heat exchanger, humidifier, and dryer are controlled through a control unit cooperating with a thermostat and a hygroscope. The control unit allows to set and maintain temperature and humidity of the conditioned air at the desired level.

Installing an additional particulate catalyst will further reduce engine power and therefore also change emissions. According to [38], tests carried out using a 1999 Honda Civic showed that removing the stock catalytic converter netted a 3% increase in horsepower. The installation of a new metallic core converter resulted in decreasing the car horsepower by 1%, as compared with case with no converter.

Therefore, it was assumed that as a result of the installation of an additional catalyst for solid particles, the power will be reduced by a maximum of 3%. Because the introduction of 2% wt. of TiO$_2$ nanoparticles to the engine oil may result in increasing the power of the engine up to 3%, may result in a situation that the measured power of the tested engine lubricated with oil containing TiO$_2$ nanoparticles can be very close to that of an unmodified engine operating in conditions close to real over the entire speed range.

According to [75], metallic additives in lube oils diminish wear and constrain sulfur-induced acidification. The metal content of fresh lube oils can be as follows: Zn 0.1–0.2%, Ca 0.5%, B 0.09%, Mg 0.002–0.004%. After prolonged deployment, the lube oil also contains abraded Fe, Cu, Pb, Mg, Al and Ni particles. For oil-consumption in the range of 1% of the fuel-consumption, the estimated Zn emission is about 1 mg/km. Moreover, Ca is emitted and all the abraded metals. Modern engines emit a tenth of that value.

The total mass of metal oxide for diesel engines is 0.1–1 mg/km, which appears negligible. But these particles are in the 10–20 nm size range. Such a small mass represents 1015 particles per kilometer, which is close to the number of soot particles emitted by diesel engines. SI engines can emit the double. These particles are emitted in the size range between 10 and 20 nm.

| Component                        | Weight M | Mass inertia moment Iz against rotation axis z |
|----------------------------------|----------|----------------------------------------------|
| Crankshaft                       | 11.887   | 0.137593                                      |
| Crankshaft sprocket              | 0.047    | 0.000007                                      |
| Outlet camshaft                  | 2.379    | 0.000341                                      |
| Outlet/inlet sprocket            | 0.165    | 0.000168                                      |
| Inlet camshaft                   | 3.822    | 0.001628                                      |
| Inlet phaser                     | 0.701    | 0.000799                                      |
| Chain                            | 2.496    | 0.002049                                      |
Metallic nanoparticles present in the exhaust can be adsorbed to other particles, e.g., soot, but in absence of this particles also nucleate by itself. Therefore, a lower soot generation at idling might lead to a higher amount of self-nucleation and is emitted as metal species (metal oxides).

There are only two ways to rectify the problem of metallic particle emission. Firstly, deploy highly efficient particle filters on all combustion engines. Secondly, diminish the metal content of the lubrication oil. The efficacy of diminishing the metal content in lube oil is proven in [10]. The filtration of ash particles from SI engines, using wall-flow catalytic converters is also possible [76].

10 Results and Discussions

The values of weights and mass inertia moment are presented in Table 3. The highest weight and the mass inertia moment had the crankshaft. The weight and mass inertia moment for the inlet camshaft were higher than for the inlet one. It was since the inlet camshaft assembly contained the heavy phaser.

The values of friction torque in the bearings are presented in Table 4. The obtained values of internal dry friction torque in the chain transmission were ca. 26% lower than the values of friction torque in the two modified crankshaft bearings containing PTFE shells.

The resulting courses of the swinging angle $\alpha$ of the chain arranged as a physical pendulum against time $t$ for different cases of friction occurring in the contact zone between fixed chain pin and mating chain roller, namely: dry, lubricated with pure engine oil and with engine oil containing 2 wt.% of TiO$_2$ nanoparticles are presented in Fig. 10. Table 5 presents the values of friction torque obtained from the pendulum swings for different friction in the contact zone between fixed chain pin and chain roller mating with it. The friction torque values in the contact zone lubricated by the engine oil were 2.5 times lower than for the dry friction. The addition of 2 wt.% of TiO$_2$ nanoparticles into engine oil 10W-40 resulted in the decrease of friction torque by about 10%.

The constants $A$ and $B$ were estimated to be equal to 14 and 1.22 s/m, respectively. Table 5 also includes the estimated values of the internal friction torque in the chain transmissions. The value of internal friction torque in the chain transmission lubricated by the engine oil was lower by 58% than in case of operation under the dry friction conditions. The

### Table 4 Calculated values of friction torque in bearings and internal friction torque in the chain transmission

| Friction torque | Values Nm |
|-----------------|-----------|
| $M_{T1}$        | 0.288174  |
| $M_{T2}$        | 0.002835  |
| $M_{T3}$        | 0.003758  |
| $M_{\text{rad}}(\omega_1 = 0.12 \text{ rad/s})$ | 0.169358 |
| $M_{\text{rad}}(\omega_1 = 0.06 \text{ rad/s})$ | 0.167130 |

### Table 5 Friction torque for different friction conditions in the contact zone

| Operational conditions in contact zone | Friction torque in the contact zone between chain pin and roller Nm | Internal friction torque in chain transmission Nm |
|----------------------------------------|---------------------------------------------------------------|-----------------------------------------------|
| Dry                                    | 0.00025                                                       | 0.169326                                       |
| Lubricated with engine oil             | 0.00010                                                       | 0.070365                                       |
| Lubricated with engine oil containing 2 wt.% amount of TiO$_2$ nanoparticles | 0.00009                                                       | 0.063768                                       |
addition of 2 wt.% of the TiO$_2$ nanoparticles into the engine oil decreased the internal friction torque by 9% in comparison to the lubrication by pure engine oil.

The addition of 2% of TiO$_2$ nanoparticles into engine oil can cause the relative changes in the engine emission as a function of engine speed. The resulting engine emissions as a function of the engine speed are presented in Table 6.

### 11 Summary

The measurement using physical pendulum swings method is the useful method for the estimation of friction torque in the contact zone between the chain pin and roller for different lubrication conditions. The internal friction torque in the chain transmission lubricated by the engine oil decreased about 58% in comparison to the case of lack of engine oil. Addition of 2 wt.% amount of the TiO$_2$ nanoparticles into the engine oil decreased internal friction torque by 9% when comparing to the case of lubrication with pure engine oil.

The frictional relationships obtained during the tests can be extended to cases of other oils differing from the tested synthetic SAE 10W-40. This requires considering extrapolative measures proposed in the paper. However, the differences regarding the composition and viscous properties of the changed oil should not be too great for the oil used during the tests.

The use of such an oil with 2% wt. of TiO$_2$ nanoparticles, in the analyzed SI engine can be related to the TiO$_2$ emission equal to $1.227\times10^{-8}$ g TiO$_2$/cycle and to 0.000012 g TiO$_2$/km. When a progressive wear of this engine occurs, its oil consumption increases which results in the emission of TiO$_2$ nanoparticles even up to 0.000006 g/km.

Based on the results obtained from a comparative analysis of emission in the other engine with similar power characteristics, the mentioned total friction losses can change the emission of the following compounds in the analyzed SI engine: 17–19% for CO, 8–9% for CO$_2$, 13–17% for NO$_x$, and 12–16% for HC. Such changes were dependent on the engine speed; the smallest changes in engine were registered for the rotation speed of 2500 rpm.

### Compliance with Ethical Standards
We declare that there are no competing interests for our article.

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