Charting the Exciton–Polariton Landscape of WSe$_2$ Thin Flakes by Cathodoluminescence Spectroscopy

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Semiconducting transition-metal dichalcogenides (TMDCs) provide a fascinating discovery platform for strong light–matter interaction effects in the visible spectrum at ambient conditions. While most of the works have focused on hybridizing excitons with resonant photonic modes of external mirrors, cavities, or nanostructures, intriguingly, TMDC flakes of subwavelength thickness can themselves act as nanocavities. Herein, the optical response of such freestanding planar waveguides of WSe$_2$ by means of cathodoluminescence spectroscopy is determined. Strong exciton–photon interaction effects that foster long-range propagating exciton–polaritons and enable direct imaging of the energy transfer dynamics originating from cavity-like Fabry–Pérot resonances are revealed. Furthermore, confinement effects due to discontinuities in the flakes are demonstrated as an efficient means to tailor mode energies, spin–momentum couplings, and the exciton–photon coupling strength, as well as to promote photon-mediated exciton–exciton interactions. The combined experimental and theoretical results provide a deeper understanding of exciton–photon self-hybridization in semiconducting TMDCs and may pave the way to optoelectronic nanocircuits exploiting exciton–photon interaction beyond the routinely employed two-oscillator coupling effects.

1. Introduction

The phenomenon of spontaneous collective coherence in condensed matter quantum systems, as most notably manifested by Bose–Einstein condensation, continues to be a subject of increasing interest.\cite{1-5} Whereas temperature is the typical control knob to drive a system of collective excitations to its ground state, quasiparticle density in solid-state systems, such as the density of plasmons\cite{6} or excitons,\cite{7,8} has recently emerged as a versatile control parameter,\cite{9} toward high-temperature condensation. In general, excitons are promising for condensation due to their light mass and bosonic nature. More specifically, excitons in semiconducting group VI transition-metal dichalcogenides (TMDCs) are advantageous because of their exceptionally high binding energies of a few 100 meV giving rise to stable and robust exciton excitations at room temperature.\cite{10-12} In addition, the high oscillator strengths associated with the excitonic resonances result in exciton lifetimes longer than 100 fs, enabling effective light–matter coupling.\cite{13} For these reasons, TMDCs are now a particularly fruitful platform for the observation of strong coupling effects between excitons and photons\cite{14} including the formation of exciton–polariton quasiparticles with effective masses reduced by several orders of magnitude.\cite{15}

To realize strong exciton–photon couplings in practice, high-quality microcavities,\cite{16-19} plasmonic nanoantennas,\cite{20} or plasmon polaritons\cite{20-22} typically need to be used. The effective interaction between cavity photons and excitons generally promotes the creation of exciton–polaritons, with spontaneous coherence enabling coherent energy transfer and the possible use in optoelectronic devices that, for example, combine ultrafast optical routing with electronics functionalities.\cite{23,24} Microcavities such as Bragg reflectors allow for a continuous tuning of the interaction strength covering weak to strong interaction regimes.\cite{25} However, the application of microcavities often involves complicated manufacturing processes, which hinders their use in hybrid electronic–optics nanocircuits. In contrast, plasmons can strongly interact with excitons via the evanescent tail of the plasmonic near-field,\cite{26} and can be used to further control the coupling strength due to the giant near-field enhancement, particularly when localized plasmons are involved.\cite{27-30} Such localized fields can be triggered by applied electric field and strongly interact with excitons, for example, in a carbon nanotube.\cite{31} In addition, plasmon–polariton dispersion and mode volume can be further controlled by structuring the materials or using metamaterials, which further affects the dispersion of the excited polaritons and the strong-coupling effects.\cite{32-34} However, plasmons themselves suffer from

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large dissipative losses and demand precise nanofabrication procedures. Therefore, simple effective platforms for strong exciton–photon coupling are in principle needed. Recently, thin TMDC waveguides were investigated along these lines by optical microscopy, spectroscopy and scanning near-field optical microscopy, where exciton–photon anticrossing behavior in individual flakes was observed and exciton–polariton propagation was directly imaged using monochromatic photons, respectively. Yet, the underlying coupling mechanisms remain largely unclear because a spectroscopic investigation at high spatial resolution and at a broad energy range is missing. Moreover, spectroscopy techniques utilizing spontaneous interactions, in contrast with laser-based techniques, could be used to unambiguously unravel the mechanism of spontaneous coherence compared to lasing.

Herein, we investigate the spontaneous optical properties of thin WSe2 flakes by means of cathodoluminescence (CL) spectroscopy. Using an electron beam-based probe, we rule out the possibility of lasing as the underlying coherence mechanism. Optical modes propagating in thin films are quasi-propagating modes, transversally confined between the film boundaries and propagating along the symmetry axis of the film. This effect results in strong exciton–photon coupling as manifested in a Rabi energy splitting of 0.24 eV (corresponding to a wavelength splitting of ≈110 nm) and the formation of exciton–polaritons whose spatial coherence and propagation mechanisms are investigated here at a high spatial resolution. Moreover, dispersion control of the optical modes via film thickness and higher-dimensional confinements, leading to excitation of edge exciton polaritons, is used to tailor the exciton–photon coupling strength. Finally, multi-oscillator coupling physics is explored on the basis of photon-mediated exciton–exciton couplings between A and B excitons, that is, polariton–polariton interactions.

2. Results

2.1. Cathodoluminescence Spectroscopy of WSe2 Waveguides

Electron microscopy has continuously been advanced as a probe of both structural and optical properties of materials, with arguably the highest spatial, temporal, and energy resolutions. Regarding the optical properties, typically either electron energy-loss spectroscopy (EELS) or CL spectroscopy are used. CL spectroscopy, in particular, has proven to be powerful in analyzing exciton and bandgap excitations in semiconductors and defects. It has only recently been revolutionized to probe not only incoherent processes but also spontaneous coherence, particularly of surface plasmon polaritons. However, the best of our knowledge, CL spectroscopy has not yet been applied to probe exciton–polariton coherence and spatial correlations, which is partially due to the competing incoherent and coherent radiation channels in semiconductors. In the following section, we will show that CL can probe exciton polaritons and Rabi splitting in atomically flat single-crystalline TMDC flakes of subwavelength thicknesses.

Specifically, we investigate the optical response of 80 nm thick flakes of the prototypical exciton-active TMDC semiconductor WSe2, using 30-keV electrons in a field-emission SEM system equipped with a parabolic mirror and optical detectors (see Experimental Section for details). Excitons are excited upon electron irradiation and exciton–photon interaction, exciton–polariton formation, as well as the propagation dynamics; which are probed by CL spectroscopy (Figure 1a). Whereas in semiconductor optics, weak exciton–photon interaction is omnipresent, strong interaction requires standing-wave-like patterns of light with increased interaction time. This is normally realized by optical cavities; where the atomically flat interfaces of a material can act as mirrors exploiting total internal reflection of the light. Such wave guiding patterns have been previously investigated using CL spectroscopy. However, to the best of our knowledge, the interaction of the waveguide modes with excitons and Rabi splitting of the excitonic states have not been investigated with CL. Thus, photonic modes of a slab waveguide, propagating within the xy-plane and forming standing-wave patterns along the transverse z-axis, facilitate both strong exciton–photon interactions and exciton–polariton transfer dynamics (Figure 1b). The corresponding WSe2 slab waveguides were fabricated by liquid exfoliation and placed on top of holey carbon transmission electron microscopy (TEM) grids (Figure 1c) or carbon discs.

2.2. Theoretical Description of Strong Exciton–Photon Coupling in WSe2 Thin Films

The coupled harmonic oscillators, underlying the strong exciton–photon interactions, are modelled by virtue of decomposing the optical responses (e.g., the permittivity of the material) versus photons captured in a slab waveguide and the Lorentzian responses associated with certain excitons; here the A and B excitons in WSe2. To better account for inhomogeneous broadening, the generalized model reported elsewhere for modelling the permittivity of the gold is adopted here as well (see Supplementary Note 1 and Figure S1, Supporting Information, for details). A dielectric slab waveguide can support optical modes of the so-called transverse electric (TE) and transverse magnetic (TM) polarizations. Within the thickness ranges considered here, the fundamental TE and TM modes are both excited; however, only the TM modes can strongly interact with the excitons and be revealed by electron spectroscopy techniques. The latter is due to the fact that electrons can only interact with those photonic modes supporting an electric-field component oriented along the electron trajectory. The photonic modes supported by a dielectric slab waveguide with $\epsilon_{\text{refr}} = 15$ can strongly interact with the A excitons in the WSe2 thin films, leading to an energy splitting and level repulsion (Figure 1d); a phenomenon often referred to as anticrossing. The resulting polariton branches, referred to as lower polaritons (LP) and upper polaritons (UP), emerge in the energy ranges below and above the A exciton energy, respectively, and exhibit rather similar group velocities. For a slab waveguide with the thickness of $d = 80$ nm, the energy gap opening is on the order of $\delta E = 0.24$ eV, $\delta \lambda = 110$ nm. In contrast to the UP branch, the attenuation constant of the LP branch for energies below 1.5 eV is sufficiently low, allowing for a propagation length of more than 8 µm, where the propagation length is determined by the field amplitude dropped by a factor $e^{-\frac{\delta \lambda}{4 \pi \mu}}$. Therefore, strong exciton–photon coupling is observed only weakly.
interactions with the higher-energy B excitons. This is due to the excitation of higher-order and yet radiative photonic channels with their dispersion diagram positioned inside the light cone, and the radiative nature of the B excitons as well, that does not allow for enhanced exciton–photon interactions. Exciton B has 3 times faster relaxation rates compared to exciton A, as can be understood by comparing $\gamma_A = 29743.43$ nm ($\tau_A \approx 99.2$ fs) to $\gamma_B = 10056.85$ nm ($\tau_B \approx 33.5$ fs) (see Supplementary Note 1 and Figure S1, Supporting Information). This effect results in much shorter interaction times between photons and the B exciton, and hence the interaction between photonic modes and the B exciton is weaker. This behavior does not depend on the thickness of the slab waveguide, but indeed lateral confinement along the y-axis can lead to the modification of the dispersion of the photonic modes, thus allowing for observing strong interactions with both A and B excitons, as will be shown later.

A momentum-resolved electron energy-loss spectroscopy (MREELS) map, calculated for an electron with a kinetic energy of 30 keV interacting with a slab waveguide of thickness $d = 80$ nm, can unravel the dispersion of propagating optical modes (Figure 1e), and demonstrates the same energy splitting and anticrossing as our model analysis predicted (see Supplementary Note 2). This demonstrates in principle the ability of swift electrons with kinetic energy as low as 30 keV (and even lower; see Figure S3, Supporting Information) to efficiently couple to exciton–polaritons in WSe$_2$ thin films and to probe their coherent dynamics. However, the required momentum resolution at lower energy-loss ranges imposes a challenge for current instruments, since the polariton-induced angular recoil experienced by the electrons covers only a few microradians for relativistic electron beams of the sort used in transmission electron microscopes. Moreover, since both radiative and loss channels contribute to EELS, probing coherent exciton–photon interactions and analysis of transport properties are less straightforward using EELS compared to CL spectroscopy (Figure 1f). In fact, the signal integrated over all the momentum components reveals that exciton absorption peaks are the dominant contributions to the overall electron energy-loss signal, for the thicknesses of interest of our thin films. In contrast, the observation of a dip—instead of a peak—at the A exciton wavelength in the CL spectra as well as a wavelength splitting as large as 110 nm demonstrates the possibility of using CL spectroscopy for probing exciton–polaritons in thin TMDC flakes. Moreover, propagating polaritons in infinite thin films normally do not contribute to the radiation channels and their dispersion line is positioned outside the light cone. Whereas the EELS signal constitutes propagating modes, the dip in the CL signal represents a depletion of energy due to the excitation of propagating modes. Interestingly, within the wavelength ranges of $749 \text{ nm} < \lambda < 774 \text{ nm}$ and $\lambda < 652 \text{ nm}$, the LP branch and higher-order radiative polaritons contribute to the radiation continuum.
(Figure 1d), whereas the photonic mode (dashed line in Figure 1d) does not. Hence, the formation of the LP mode and the strong coupling effect result in two CL peaks, in contrast to the exciton absorption peak apparent in the EELS signal.

A deeper understanding of the level repulsion phenomenon in quantum electrodynamics systems, and the resulting Rabi oscillations, demands a more rigorous treatment of light–matter coupling. Herein, we comply with a simple semi-classical model that perfectly captures the main mechanisms, defining the coupling between the electric field \( \vec{E} \) of the photonic modes and the macroscopic exciton polarization \( \vec{P} \) as:\[^{[13]}\]

\[
\begin{align*}
\dot{\vec{P}} &= (\omega_{\text{ex}} - i\gamma)\vec{P} + g\vec{E} \\
\dot{\vec{E}} &= (\omega_{\text{ph}} - i\kappa)\vec{E} + g\vec{P}
\end{align*}
\] (1)

where \( \omega_{\text{ex}} \) and \( \omega_{\text{ph}} \) are the angular frequencies of the exciton and photon oscillators, \( \gamma \) and \( \kappa \) are their damping constants, \( g \) is the coupling strength, and time derivative is indicated by a dot on top. The eigenfrequencies of the coupled system of equations in Equation (1) are derived by assuming time-harmonic responses (\( P = P_0 \exp(\mathrm{i} \omega t) \) and \( E = E_0 \exp(\mathrm{i} \omega t) \)) and are given by

\[
\alpha_n = \frac{1}{2} (\omega_{\text{ph}}(k) + \omega_{\text{ex}} - i(\gamma + \kappa)) \pm \frac{1}{2} \sqrt{\Delta}
\] (2)

with

\[
\Delta = (\omega_{\text{ph}}(k) - \omega_{\text{ex}})^2 + 2\Gamma\omega_{\text{ph}}(k)\omega_{\text{ex}} - (\gamma - \kappa)^2 + i2(\omega_{\text{ph}}(k) - \omega_{\text{ex}})(\gamma - \kappa)
\] (3)

and \( \Gamma = 2g^2(\omega_{\text{ph}}\omega_{\text{ex}})^{-1} \). Equation (2) defines two solutions for the system associated with the LP and UP branches. Going beyond previous works, we allow for nonzero damping terms, thus the complex-valued parameter \( \Delta \) can be used to model both Rabi oscillation and its damping. Intriguingly, for the resonance condition \( (\omega_{\text{ph}}(k) = \omega_{\text{ex}}) \), the damping of the Rabi oscillation is only determined by the damping of its underlying oscillators as \( \text{Im} (\alpha_n) = -(\gamma + \kappa)/2 \). In contrast, detuning of the energy \( \hbar\delta\omega = \hbar\omega_{\text{ex}} - \hbar\omega_{\text{ph}} \) can cause another mechanism for the relaxation of the Rabi oscillation. We have assumed a dispersion-dependent model for the photonic mode, allowing for efficient modeling of the anticrossing behavior similar to the complete treatment in Figure 1d. Using the extracted parameters for the A exciton energy and photonic modes \( (\omega_{\text{ex}} = 1.65 \text{ eV}, \gamma = 0.0417 \text{ eV}, \text{ and } \kappa = 0; \) see Supplementary Note 1), and under resonance condition \( (\omega_{\text{ph}}(k) = \omega_{\text{ex}}) \), we indeed observe an energy splitting \( \Omega = \omega_{\text{ex}} - \omega_{\text{ph}} \) of 0.24 eV for a coupling strength of \( g = 121 \text{ meV} \). A slightly larger coupling efficiency of \( g = 163 \text{ meV} \) has been reported for WS2 nanotube waveguides, which offer a more confined modal configuration and hence stronger exciton–photon interactions.

2.3. Experimental Probing of Exciton–Polaritons Using CL Spectroscopy

In the experiments, we first look at the CL response of a WSe2 flake with a thickness of 80 nm (Figure 2). CL spectra, acquired at selected electron impact positions, demonstrate a wavelength

![Figure 2](image-url)
splitting on the order of 120 nm, comparable to the predicted values, and a dip at the A exciton wavelength of 751 nm (Figure 2c). This splitting is fully reproduced in the calculated CL spectra (Figure 2g). Upon scanning the electron beam vertically to the edge of the flake, we observe several maxima with their relative distance depending on the wavelength (as indicated by the dashed arrows in Figure 2b), and a dip at the A exciton energy splitting the excited polaritons into energy intervals above and below the exciton A energy associated with UP and LP branches, respectively. The energy of the photonic mode depends on the thickness of the slab waveguide. Hence, the exciton–phonon coupling strength and the observed energy splitting strongly depend on the thickness of the slab waveguide (Figure 2d). For a slab waveguide at a thickness of 65 nm, the splitting in the wavelength is on the order of \( \Delta \lambda = 250 \text{ nm} \), whereas by increasing the thickness to 80 nm, the wavelength splitting becomes \( \Delta \lambda = 120 \text{ nm} \). The increase in the wavelength splitting is understood by generating more resonant conditions between photons and excitons (Figure 5, Supporting Information). Nevertheless, for larger thicknesses, the excitation of higher-order modes and the Cherenkov radiation result in exciton–phonon interactions as well (Figure 7, Supporting Information).

When comparing to the results of numerical calculations (using the finite-difference time-domain method, see Experimental Section), we indeed observe peaks at the predicted spectral and spatial positions in the 2D CL spectrum. However, the maximum–minimum contrast, in the experimental data is less pronounced, which we attribute to structural imperfections, potentially caused by our liquid exfoliation and chemical inhomogeneity.

Hyperspectral images at selected photon wavelengths capture the spatially resolved standing wave patterns, parallel to the edges (Figure 3c). This can be understood as the constructive interference between the TR and the diffraction of the excited exciton–polaritons from the edges of the flakes at the far field. Therefore, a constructive interference pattern can be formed by the excitation of the surface exciton–polaritons with phase fronts parallel to the edges (Figure 3d). The observed peaks in the CL energy–distance maps are broad, due to the dissipative losses associated with the TE mode. The propagation constant of the slab modes can be decomposed into their real (\( \beta_{EP} \)) and imaginary parts (\( \alpha_{EP} \)), corresponding to the phase and attenuation constant, respectively (Figure 3e). The relatively large attenuation constant for the TM\(_x\) mode at the measured photon energies is the reason for the large broadening of the peaks in the distance–wavelength CL map. Indeed, the calculated attenuation constant at the wavelength ranges from 550 to 600 nm is larger than the phase constant, confirming the diminishing role of the spatial interference fringes in the experimental results within this range. The excited exciton–polaritons at these wavelengths are strongly attenuated and cannot propagate at spatial ranges larger than the wavelength; therefore, spatial interferences cannot be observed. To reveal the phase constant from the energy–distance CL map, the distance between the peaks is measured at selected wavelengths as \( D(\lambda_0) \) and related to the phase constant by \( \beta_{EP}(\lambda_0) = 2\pi / D(\lambda_0) \cos \theta \) (see Figure 3d). A direct comparison between the calculated surface exciton–polariton dispersions and measured spectral and spatial fringes reveals a good agreement with the TM\(_x\) mode, supporting our second hypothesis (Figure 3e).

The aforementioned dominance of the hypothesis, compared to the spatial interference patterns caused by the reflection from the edges, is due to the larger transmission coefficients of guided waves compared to the reflection coefficients at the edges of the flakes. The reflection and transmission coefficients are largely material-dependent quantities and also depend on the geometry of waveguiding discontinuities. Hence, either the first or second scenario has been used in the literature for describing the observed spatial interference fringes in various materials and flake geometries.\(^{38,51}\)
Our findings places CL spectroscopy parallel to scanning near-field optical microscopy, as a direct measure of spatially and spectrally resolved polaritonic transport mechanisms. However, a better agreement can only be provided by considering edge exciton–polaritons as an individual transport mechanism parallel to surface polaritons, as will be discussed in the subsequent section.

### 2.4. Edge Exciton–Polaritons

Edge polaritons, in contrast to surface polaritons, are spatially confined to and propagate along the pristine edges of the flakes. The spatial confinement and different screening mechanism of edge exciton–polaritons compared to bulk excitons lead to lower attenuation constants and shifted exciton energies. By scanning the edge of a WSe$_2$ flake with a trapezoidal geometry (Figure 4a), spatial interference fringes of up to several orders are observed (Figure 4b), due to lower attenuation constants compared to surface polaritons.

The Fourier-transformed CL map allows for acquiring the dispersion of the edge exciton–polaritons (Figure 4c). The Fourier transformation is performed by using the discrete Fourier transformation method within the MATLAB environment. A bright intensity at $k_\parallel = 0$ is caused by the background noise, and particularly non-propagating evanescent modes with high attenuation constants. Those higher-order modes strongly contribute to the dissipation of the energy delivered by the excitation source without contributing to the desired spatial coherence associated with the propagating optical waves. In addition, however, a pronounced signal with the momenta lying outside the light cone is observed. Theoretical modelling of the propagating edge exciton–polaritons are performed by calculating the optical modes supported by a rectangular rib waveguide, with the width and height of 500 and 100 nm, respectively. The fundamental mode of this rib waveguide has optical mode profiles confined to the edges of the waveguide (Figure 4e). Interestingly, although the $E_y$ field component is mostly concentrated inside the channel waveguide, the $E_z$ component is concentrated along the edges. Since the $E_z$ component couples strongly to the electron beam excitation, the spatial profile of the CL signal is dominated by the spatial profile of the $E_z$ field component. Moreover, due to the dominance of the $E_z$ field strength over the $E_y$ component, the overall intensity of the field is concentrated in the free-space region around the edges, resulting in a lower attenuation constant of the edge polaritons compared to the surface polaritons (Figure S2, Supporting Information). Several higher-order optical modes exist with field profiles confined to the edges and surfaces of the flakes. However, only the fundamental mode is experimentally captured, as understood by comparing the calculated dispersion diagram of the fundamental mode and the experimental results (Figure 4c; solid lines). Hyperspectral images demonstrate the spatial profile of the excited edge exciton–polaritons and also unravel the ultra-confined mode volumes associated with these modes (Figure 4d). This is understood by observing that the spatial profile of the CL maps at demonstrated energies are highly confined to the edges of the flakes. Indeed, the evanescent tails of the edge exciton–polaritons at the photon

![Figure 3. Propagation mechanisms of the upper branch of the exciton–polaritons.](image-url)
energy of 2.06 eV (\(\lambda = 600 \text{ nm}\)) are \(\kappa^{-1} = 16\) and 22 nm, for fields penetrating into the vacuum and inside the flake, respectively. This is calculated by integrating the acquired CL map along the \(x\)-axis, and fitting the data to \(c_1 + c_2 \exp(-2\chi |y - y_0|)\), where \(y_0\) is the location of the edge along the \(y\)-axis, and \(c_1\) and \(c_2\) are fitting coefficients accounting for the background noise (and spatially incoherent contributions) and exciton–polaritons, respectively.

### 2.5. Photon-Mediated Exciton–Exciton Interactions

Natural layered flakes with step edges, allowing for lateral confinements of the photonic modes, provide a natural mechanism for further tuning the energy and modal configurations of the photonic excitations (see Figure 5a). Particularly in those flakes, we indeed observe not only an omnipresent dip in the CL spectra at the wavelength associated with the A exciton, but also a series of peaks and dips in the wavelength range of the UP branch (Figure 5b,c). These spectral fringes are revealed in numerical simulations as well (Figure 5d), in a good agreement with experimental results.

Higher-order photonics modes of a slab waveguide can cause oscillations in the LP range, but they cannot result in the spectral fringes we observe in the UP range. Moreover, Cherenkov radiation (CR) caused by an electron moving inside a bulk material can strongly interact with the excitons, similar to the photonic modes of the slab waveguide (see Supplementary Note 2 and Figure S5, Supporting Information). CR can be excited and captured inside thick films with \(d > 400\) nm, and can be further released to the far-field zone by virtue of its interaction with discontinuities. However, our theoretical and experimental CL analysis rules out the possibility of observing spectral fringes in the UP branch that can be related to either photonic modes or CR. Another possible origin of the observed additional spectral peaks could be due to the excitation of trions or higher-order modes. We rule out those possibilities as well, as our simulations using the permittivity data dominated by only two exciton A and B resonances perfectly reproduce the experimentally observed spectral peaks.

To better understand the mechanisms underlying the oscillations we observe for the UP branch, we propose a model based on photon-mediated exciton–exciton interactions. Generally, a system of two coupled oscillators is used to describe the strong-coupling effects. As extensively discussed previously, the strong-coupling phenomenon leads to the hybridization of the excitonic states and thus two peaks instead of a single exciton peak are observed in the measured spectra. Thus, the appearance of more than two peaks in the measured spectrum (Figure 5c) could be associated with the coupling between more than two oscillators: exciton A, exciton B, and photons. To test the proposed hypothesis, we provide the mathematical form of the three coupled-oscillators model. Equation (1) can be modified to include photon-mediated couplings between the A and B excitons (Figure 6a), by...
where a system of three coupled harmonic damped oscillators is considered (Figure 6b). In a similar approach to the aforementioned one, here we fix the values for \( \omega_{\text{ex}, A}, \omega_{\text{ex}, B}, \gamma_{\text{ex}, A}, \) and \( \gamma_{\text{ex}, B}, \) as well as \( \omega_{\text{ph}} \) and \( \kappa \) by the values provided in the supplementary Note 1. Hence, only \( g_1 \) and \( g_2 \) remain as fitting parameters. The time-harmonic response of this coupled system of equations represents three eigenvalue solutions to the system, the values of which can be tuned by \( \omega_{\text{ph}} \). We express these eigenvalues by \( \omega_i \) where \( i = 1, 2, 3 \) (Figure 6c). We indeed assume that excitons A and B can only indirectly interact with each other, by virtue of exchanging photons. Therefore, only two coupling coefficients between the photonic modes and the exciton peaks are considered. By considering the coupling coefficients \( g_1 = 26.3 \text{ meV} \) and \( g_2 = 65 \text{ meV} \), we observe a strong shift of the second eigen-wavelength from 610 to 730 nm, by reducing the frequency of the photonic mode from 2.2 to 1.6 eV (blue line, Figure 6c). For \( \omega_{\text{ph}} < \omega_{\text{ex}, A} \), we observe a strong red shift of the third eigenvalue by reducing further the photon energy (Figure 6c, red line). By assuming a Lorentzian line shape centered at each calculated eigenvalue, we reveal an overall spectral shape that is in good agreement with the measured and simulated results represented in Figure 5c,d, respectively. Moreover, though in general four spectral peaks are apparent in the acquired CL data, we notice that the system of three coupled oscillators is sufficient to lay open the underlying mechanism, since the additional middle peak at the wavelength of \( \lambda = 660 \text{ nm} \) can be understood by the overlapping tails of adjacent green and blue resonances (Figure 6d); while the overlapping tails of the blue and red resonances are not able to create an additional middle peak. This is due to the significant role of inhomogeneous broadening that dominates the shape of the exciton B resonance.

3. Discussion

The cathodoluminescence response of semiconductors is naturally understood per excitation of many electron–hole pairs, where the statistical distributions of the generated photons do not resemble coherent photon statistics. We indeed ascertain that the presence of spontaneous coherence supported by the excitation of exciton–polaritons, provides evidence for CL spectroscopy to be able to probe Rabi oscillations and nonlinear exciton–photon interactions. In addition and in an inverse approach, semiconductors with room-temperature exciton excitations like TMDCs can be used to generate both X-ray photons and coherent visible-range photons upon electron irradiation, and thus provide a means for designing electron-driven photon sources of higher photon yield compared to plasmonic structures.[64] Performed simulations, particularly when compared to the experimental results, confirm the formation of exciton–polaritons and their coherence statistics. Both spatial and spectral profiles are well represented in our numerical results confirming

Figure 5. Photon-mediated exciton–exciton interactions. a) Dark-field SEM image of the investigated flakes. b) CL wavelength–distance map, demonstrating three finer structure peaks in the UP band, caused by three oscillator couplings (see text and Figure 6). The vertical axis is the scanning range of the electron beam, shown by the red box in panel (a). Measured (c) and simulated (d) spectra at selected electron impact positions indicated in panel (b).
the accuracy of the permittivity model and the dominance of the classical broadenings. However, we observe deviations from the experimental results that might be due to the exciton dephasing dynamics; which needs to be confirmed by more demanding quantum theories.\cite{65} Moreover, numerical constraints regarding the simulation time and domain, normally do not allow us to consider comparable structural sizes particularly when an infinitely long slab waveguide is considered (Figure 2). Thus, the response of the truncated slab waveguide at the size of 2 μm deviates from the 10 μm-long slab employed in the experiments.

Although our results demonstrate evidence for photon-mediated exciton–exciton interactions in natural flakes, related to the energy relaxation between excitonic states, further control of the coupling mechanisms by nanostructuring and controlling the temperature will provide a toolbox for better understanding the formation of long-range spatial correlations associated with Bose–Einstein condensation.\cite{66}

The Stokes shift between the luminescence and absorption peaks will result in a shift of the CL peaks compared to EELS spectra.\cite{67} However, this effect has been shown to cause only a minor effect compared to the strong-coupling effects we observe here, for nominally undoped materials, whereas it can be significantly increased for n-doped materials.\cite{68} The short interaction of the electron beam with our structure does not cause any significant sample heating or doping, as the positions of the peaks do not depend on the acquisition time, the acceleration voltage within the range of 5 to 30 keV, and also not on the probe current within the range of 10 to 20 nA (see Figure S6, Supporting Information). We, therefore, conclude that the possible Stokes shift has a negligible effect compared to the effect of strong exciton–photon interactions on the spectra. In summary, we demonstrated strong coupling between excitons of WSe2 and the propagating photons of freestanding thin WSe2 flakes with a Rabi splitting on the order 0.24 eV. The overall energy–momentum EELS map and cathodoluminescence spectroscopy results show anticrossing of upper and lower polariton branches and long-range propagation of exciton–polaritons in high-quality atomically flat flakes. Additionally, the possibility of controlling photon-mediated exciton–exciton interactions via excited photonic modes in optoelectronic nanocircuits is another intriguing feature of thin-film van der Waals materials. Our results thus reveal that the coupling strength of photon-mediated exciton–exciton interactions in atomically flat WSe2 flakes can be further controlled by tuning the energy and field profiles of photonic modes.

4. Experimental Section

Synthesis and Exfoliation of Single-Crystalline WSe2 Crystals: Single crystals of 2H-WSe2 were grown by the standard chemical vapor transport method: A near-stoichiometric mixture of high-purity W and Se with a slight Se excess (4 mg cm\(^{-2}\)) was placed in a quartz ampoule together with iodine.
calculate the scattered field allows for improving the accuracy compared to the experimental results.

To calculate the EELS and CL, in the frequency domain, we employed the radiofrequency (RF) toolbox of COMSOL in a 3D simulation domain, where the Maxwell equations are solved in real space and in the frequency domain. We utilized an oscillating “Edge Current” as a fast electron beam along a straight line representing the electron beam. The current was expressed by $I = I_0\exp(i\omega t/\nu_0)$. The CL was calculated by using boundary probe at a plane normal to the electron beam. The dielectric function of WSe$_2$ was defined using the interpolation function of COMSOL. We applied the free tetrahedral mesh with denser elements close to the electron trajectory. The size of the mesh elements toward outer boundaries were increased. Additionally, we used perfectly matched layers (PML) to prevent unphysical field reflections from the boundaries.

**Supporting Information**

Supporting Information is available from the Wiley Online Library or from the author.

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**Conflict of Interest**

The authors declare no conflict of interest.

**Author Contributions**

M.T. has performed the CL measurement and data analysis, and fabricated the thin film samples. F.D. and N.T. have performed the simulations. F.K.D. and K.R. have provided the bulk crystals. N.T. and K.R. have written the manuscript. All co-authors have contributed to discussions. N.T. supervised the work.

**Data Availability Statement**

Research data are not shared.

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