FRAGMENTATION OF MASSIVE DENSE CORES DOWN TO $\leq 1000$ AU: RELATION BETWEEN FRAGMENTATION AND DENSITY STRUCTURE*

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ABSTRACT

In order to shed light on the main physical processes controlling fragmentation of massive dense cores, we present a uniform study of the density structure of 19 massive dense cores, selected to be at similar evolutionary stages, for which their relative fragmentation level was assessed in a previous work. We inferred the density structure of the 19 cores through a simultaneous fit of the radial intensity profiles at 450 and 850 μm (or 1.2 mm in two cases) and the spectral energy distribution, assuming spherical symmetry and that the density and temperature of the cores decrease with radius following power-laws. Even though the estimated fragmentation level is strictly speaking a lower limit, its relative value is significant and several trends could be explored with our data. We find a weak (inverse) trend of fragmentation level and density-power-law index, with steeper density profiles tending to show lower fragmentation, and vice versa. In addition, we find a trend of fragmentation increasing with density within a given radius, which arises from a combination of flat density profile and high central density and is consistent with Jeans fragmentation. We considered the effects of rotational-to-gravitational energy ratio, non-thermal velocity dispersion, and turbulence mode on the density structure of the cores, and found that compressive turbulence seems to yield higher central densities. Finally, a possible explanation for the origin of cores with concentrated density profiles, which are the cores showing no fragmentation, could be related with a strong magnetic field, consistent with the outcome of radiation magnetohydrodynamic simulations.

Key words: galaxies: star clusters: general – radio continuum: ISM – stars: formation – techniques: high angular resolution

Online-only material: color figures

1. INTRODUCTION

One unavoidable ingredient in the process of formation of intermediate-/high-mass stars is that they are usually found associated with clusters of lower-mass stars (e.g., Lada & Lada 2003; Rivilla et al. 2013). However, the process yielding the formation of these clusters is not clear, as it remains ambiguous how a cloud core fragments to finally form a cluster. The observed star formation efficiency is by far much smaller than the predicted if gravity dominated the dynamics of the collapse (see, e.g., Kruithoff 2013 for a review), and the number of subcondensations typically embedded in massive dense cores is again smaller by one order of magnitude than the predicted from a pure Jeans fragmentation analysis (e.g., Hennemann et al. 2009; Zhang et al. 2009; Zhang & Wang 2011; Bontemps et al. 2010; Longmore et al. 2011; Pillai et al. 2011; Wang et al. 2011; Lee et al. 2013). Thus, a broad observational evidence indicates that additional physical ingredients competing with gravity must play an important role in the fragmentation process, such as angular momentum, stellar feedback, magnetic fields, and turbulence.

Numerical simulations are becoming crucial to establish the relative importance of each of these ingredients in the fragmentation process. Simulations of fragmentation of rotating cores with different equations of state show that cores with some angular momentum easily fragment into multiple objects (e.g., Boss & Bodenheimer 1979; Bate & Burkert 1997) and thus need additional mechanisms to decrease the fragmentation down to the observed levels (see Goodwin et al. 2007 and references therein). A crucial ingredient in this sense is the presence of a magnetic field. Studies on the effects of magnetic fields in the evolution of a collapsing and rotating core indicate that a strong magnetic field can suppress fragmentation as it constitutes an additional form of support and also via the so-called magnetic
braking (e.g., Hosking & Whitworth 2004; Mellon & Li 2008; Hennebelle & Teyssier 2008), which is very effective in removing a significant part of the initial angular momentum through torsional Alfvén waves. Similarly, radiation magnetohydrodynamic simulations of turbulent massive dense cores show that the combined effects of radiative feedback (e.g., Krumholz et al. 2007; Peters et al. 2011) and magnetic field can sum to efficiently suppress fragmentation (e.g., Hennebelle et al. 2011; Commerçon et al. 2011; Myers et al. 2013), yielding a better match with the observations (e.g., Palau et al. 2013). In addition, submillimeter observations show that the magnetic field is important in the dynamical evolution and fragmentation of massive dense cores (e.g., Girart et al. 2009, 2013; Hezareh et al. 2013). Another ingredient probably playing a role in the fragmentation process is supersonic turbulence. Theoretical studies show that turbulence generates density structures due to supersonic shocks that compress and fragment the gas efficiently, especially for large Mach numbers (e.g., Padoan et al. 2001, Schmeja & Klessen 2004; Vázquez-Semadeni et al. 2007). More recently, it has been shown that the turbulence mode, solenoidal, or compressive (e.g., Vazquez-Semadeni et al. 1996; Federrath et al. 2008), differently affects the cloud structure and fragmentation. Solenoidal turbulence corresponds to a null divergence of the driving force (divergence-free) and arises from galactic rotation and magneto-rotational instabilities, and seems to be at work in the Rosette and Polaris Flare clouds (e.g., Hily-Blant et al. 2008; Federrath et al. 2010). Compressive turbulence corresponds to a null curl of the driving force (curl-free) and can be produced by expanding supernova shells or H ii regions (e.g., Federrath et al. 2010), as seen in the Pipe Nebula and the Orion B cloud (Peretto et al. 2012; Schneider et al. 2013). Numerical simulations comparing both types of turbulence indicate that compressive turbulence promotes fragmentation and generates high density contrast structures, while solenoidal turbulence slows fragmentation down and keeps a smooth density structure in the cloud (e.g., Federrath et al. 2010; Girichidis et al. 2011).

In addition to these physical agents opposing to gravity, the outcome of numerical simulations also depends on the geometry and physical properties of the collapsing core, in particular the density profile. Hydrodynamical simulations show that highly concentrated cores (e.g., \( n_{\text{H}} \propto r^{-2} \)) lead to the formation of one single massive star, while flat density profiles (\( n_{\text{H}} \propto r^{-1} \) or flatter) produce an important number of low-mass stars (e.g., Myhill & Kaula 1992; Burkert et al. 1997; Girichidis et al. 2011). This trend appears to be seen in high-resolution observations of IRDC G28.34+0.06, where three massive dense cores with different density profiles show varying degrees of fragmentation (Zhang et al. 2009; Wang et al. 2011). Finally, the substructure of molecular gas within a dense core is decreasing with time as the core turns gas into stars, as shown for example by Smith et al. (2009).

From an observational point of view, most of the studies focusing on fragmentation of massive dense cores deal with single regions and/or do not reach high enough spatial scales to study individual fragments in the core (\( \sim 1000\text{--}2000 \) AU; e.g., Longmore et al. 2011; Pillai et al. 2011; Miettinen 2012; Beuther et al. 2013; Kinunen & Tan 2013; Takahashi et al. 2013). Recently, Bontemps et al. (2010) studied a sample of six massive dense cores in Cygnus X and conducted a consistent analysis for all the regions, finding cores with a variety of fragmentation levels. A subsequent study by Palau et al. (2013) focused on a list of 18 massive dense cores (including Bontemps et al. 2010 sources), which were observed with similar spatial resolution (\( \sim 1000 \) AU), sensitivity (down to \( \sim 0.3 \mu \text{Jy} \)), and field of view (\( \sim 0.1 \) pc of diameter), again revealed different fragmentation levels, with about \( \sim 30\% \) of the regions showing no fragmentation at all. Palau et al. (2013) studied possible correlations between the fragmentation level and properties of the cores such as mass, average density, evolutionary indicators, rotational-to-gravitational energy, and turbulent velocity dispersion (although these last two properties should be studied in a larger sample) and found no clear trend of fragmentation level with any of these core properties. In that work, two main properties of the cores remained to be studied in relation to fragmentation, mainly the magnetic field and the density structure. While the magnetic field cannot currently be assessed in this sample in a uniform way, the density structure has been studied in roughly half of the sample (e.g., Beuther et al. 2002; Mueller et al. 2002; Crimier et al. 2010; van der Tak et al. 2013) but the methodology used is different for each work, casting some doubt on the validity of any comparison. Here, we present a uniform study of the density structure of each core in the sample of Palau et al. (2013), aiming at accurately assessing its impact on the fragmentation level.

In Section 2, we present the sample of cores and the data used to extract the submillimeter intensity profiles and the spectral energy distributions (SEDs), and we also present the envelope model used to fit these data simultaneously for each core. In Section 3, we present the results of our fits. In Section 4, we discuss the possible trend between fragmentation level and density structure. Finally, in Section 5, we summarize our main conclusions.

2. DATA AND METHODOLOGY

2.1. Data

We aim at studying the density structure of the 18 massive dense cores presented in Palau et al. (2013) plus DR21-OH, a massive dense core for which fragmentation has been recently studied at similar mass sensitivities and spatial resolution by Girart et al. (2013). Among the total number of 19 massive dense cores, 16 of them are identified as submillimeter sources in the catalog of Di Francesco et al. (2008) and thus have James Clerk Maxwell Telescope (JCMT) 850 and 450 \( \mu \text{m} \) data available (see Di Francesco et al. 2008 for a detailed description on the observations). For the three cores not included in the Di Francesco et al. catalog, IRAS 22198+6336, CygX-N12, and CygX-N63 (following labeling of Bontemps et al. 2010), we used the submillimeter data of Jenness et al. (1995), who also observed the 450 and 850 \( \mu \text{m} \) emission with the JCMT, and the IRAM 30m 1.2 mm data from Motte et al. (2007). The beam (main+error) of the JCMT data was taken from Di Francesco et al. (2008), and the beam (main+error) of the IRAM 30 m telescope at 1.2 mm was taken from Greve et al. (1998). Three regions for which the 450 \( \mu \text{m} \) data from Di Francesco et al. (2008) were not usable were downloaded from the JCMT archive (IC1396N: m98bu24; AFGL5142: m96bc57; W3IRS5: m02ac32). The single-dish images at 450 and 850 \( \mu \text{m} \) (1.2 mm) for the 19 cores, together with the interferometric images showing the fragmentation in each core, are shown in the Appendix (Figures 10–13).

In order to characterize the spatial structure of the massive dense cores, we computed the circularly averaged radial intensity profile, in rings of 4\( ^{\prime} \) width, as a function of the projected distance from the core center at both 850 and 450 \( \mu \text{m} \) when possible, and applied the model described in Figure 1.
and Section 2.2. The intensity profiles at 850 and 450 μm are shown in Figures 2–5. As can be seen in the figures, the emission is partially resolved for all the cores, revealing the existence of an envelope of decreasing intensity with radius, even at small distances (≲10′′) from the core center. In some cases, the radial profile was calculated in particular angular “sectors” centered on the core peak, to avoid strong negative emission in the maps (NGC 7129-FIRS2 at 450 μm), or contamination from a nearby strong core (W3IRS5) or from the DR21 ridge (CygX-N48, CygX-N53, DR21-OH). For these cases, we did not use the values of the flux density at 850 and 450 μm listed in Di Francesco’s catalog but remeasured the flux densities to assure that we were not including emission from the nearby cores/ridge. For the case of W3IRS5, the sector was taken in the north-south direction also to avoid possible contamination of free–free emission from strong centimeter sources.15 For the case of CygX-N48, we extracted the intensity profile avoiding the contribution from the north, although Richardson et al. (1989b) estimated the contamination from free–free emission to be <25% at 1.1 mm, and only <3% at 800 μm, the centimeter sources A and B reported by Tieftrunk et al. (1997) are spatially overlapping the core emission and we prefer to avoid them.

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where the strong DR21-OH core lies; for DR21-OH and CygX-N53, we extracted the profile in a sector with no restrictions in the east–west direction but allowed it to extend $\sim \pm 25''$ in the north–south direction, which corresponds to the approximate width of the DR21 filament in the east–west direction.

The SED of each massive dense core was built from centimeter wavelengths up to 50–60 $\mu$m, as this is approximately the wavelength where envelope and disk contributions start to be comparable (e.g., Crimier et al. 2010; Commerçon et al. 2012), and here we only model the envelope contribution. To build the SEDs, we used the data compiled in Palau et al. (2013), which included flux densities at different frequencies from IRAS, JCMT/SCUBA, AKARI, and IRAM 30 m data when available. In addition, we measured the flux densities at 70 $\mu$m of cores with available Spitzer/MIPS2 data. Flux densities obtained in heavily saturated Spitzer/MIPS2 data were considered as lower limits. We also considered as lower limits the millimeter/submillimeter flux densities measured with an interferometer, as part of the core emission is filtered out and we did not take this into account in our model. For OMC-1S, we recomplied the SED because the SED in Palau et al. (2013) was built for the source 136–355 (about $\sim 12''$ north of the submillimeter peak), while now we have considered the fluxes associated with the submillimeter peak, as we are modeling the submillimeter profiles. In addition, we used the FIR/submillimeter/centimeter fluxes from the literature.16 The apertures where fluxes were assessed were figured out from the literature or adopted as reported

16 IC1396N: Saraceno et al. (1996), Beltrán et al. (2002b), Codella et al. (2001), E2198: Sánchez-Monge (2011); NGC 2071: Butner et al. (1990); NGC 7129: Eiroa et al. (1998), Fuente et al. (2001), Crimier et al. (2010); CB3: Launhardt et al. (1997); OMC1-S: Jaffe et al. (1984), Lis et al. (1998), Goldsmith et al. (1997), Zapata et al. (2004a, 2004b); AFGL5142: Zhang et al. (2007), Hunter et al. (1999), Sánchez-Monge (2011); I05358NE, I22134: Beuther et al. (2002, 2007), Sánchez-Monge (2011); I20126: Cesaroni et al. (1997, 1999, 2005), Hofner et al. (1999), Sánchez-Monge (2011); HH80: Fernández-López et al. (2011); W3IRS5: Campbell et al. (1995), Richardson et al. (1998b); AFGL 2591: van der Tak et al. (1999), van der Tak & Menten (2005); CygX-N53, N12, N63 and N48: Duarte-Cabral et al. (2013); DR21-OH: Harvey et al. (1986), Gear et al. (1988), Richardson et al. (1989a), Motte et al. (2007), Araya et al. (2009), Zapata et al. (2012).
2.2. Model

We modeled the thermal emission of the cores at millimeter and submillimeter wavelengths with a spherically symmetric envelope of gas and dust, with density and temperature decreasing with radius. The density and temperature were assumed to be power-laws of radius, with indices \( p \) and \( q \), \( \rho = \rho_0 (r/r_0)^{-p} \) and \( T = T_0 (r/r_0)^{-q} \). For the dust opacity law, we assumed that the dust opacity is a power-law of frequency with index \( \beta \), \( \kappa_\nu = \kappa_0 (\nu/\nu_0)^\beta \), where \( \nu_0 \) is an arbitrary reference frequency. The values used for the dust opacity were those of Ossenkopf & Henning (1994), for thin ice mantles at a gas density of \( 10^6 \text{ cm}^{-3} \), i.e., \( \kappa_0 = 0.008991 \text{ cm}^{-2} \text{ g}^{-1} \) for \( \nu_0 = 230 \text{ GHz} \), being \( \beta \) a free parameter of the model.

In the case of optically thin dust emission, in the Rayleigh–Jeans approximation, and for an infinite radius envelope, the intensity as a function of the projected distance to the source center, \( I_\nu(b) \), can be derived analytically (see, for instance, Beltrán et al. 2002a) and is a power-law of the projected distance to the envelope center \( b \), \( I_\nu(b) \propto b^{1-(p+q)} \), with index \( 1-(p+q) \).

In our model, however, none of the above approximations (optically thin, Rayleigh–Jeans) were made, and there is no analytical expression for the intensity profile. In general, the contribution to the radiated intensity from an element of the envelope of geometrical depth \( dz \), at a radius \( r \) from the center (see Figure 1) is given by

\[
dI_\nu = \frac{dI_\nu(r)}{dz} = \frac{2k\nu^2}{c^2} J_\nu[T(r)] e^{-\tau_\nu(b,z)} \rho(r) \kappa_\nu dz,
\]

where

\[
\tau_\nu(b,z) = \int_{-\infty}^{z} \rho(r) \kappa_\nu dz',
\]

with \( r = \sqrt{b^2 + z^2} \), is the optical depth from the observer to the element of the envelope at a projected distance \( b \) and position \( z \)
Figure 5. Same as Figure 2 for the last four cores of Table 1. For CygX-N12 and CygX-N63, the profiles were extracted from the 1.2 mm images of Motte et al. (2007). (A color version of this figure is available in the online journal.)

along the line of sight (see Figure 1), and $J_\nu(T)$ is the Planck function in units of temperature,

$$J_\nu(T) = \frac{h \nu}{k} \exp\left(\frac{h \nu}{kT}\right) - 1.$$  \hfill (3)

Then, the resulting intensity as a function of the projected distance to the source, $I_\nu(b)$, has to be evaluated as

$$I_\nu(b) = \int_{z_{\text{min}}}^{z_{\text{max}}} \frac{dI_\nu(r)}{dz} dz,$$ \hfill (4)

where $z_{\text{max}} = \sqrt{b^2 + r_{\text{max}}^2}$ and $r_{\text{max}}$ is the maximum radius where the model is calculated. The computational burden is low, since both integrals, those of Equations (2) and (4), can be evaluated simultaneously in a single run.

Regarding the temperature distribution of the envelope, Chandler et al. (1998) derive from the expressions of Scoville & Kwan (1976) that, for the radiative heating of a dust cloud by a central luminous source, the temperature power-law index $q$ is a function of the dust emissivity index $\beta$, $q = 2/(4 + \beta)$. However, for the outer part of the envelope, the external heating can be important, and a constant temperature of 10 K was adopted for radii larger than the radius where the temperature distribution of index $-q$ drops to 10 K. Regarding the density distribution, we adopted, as maximum radius of the envelope $r_{\text{max}}$, the radius for which the envelope density dropped to a value comparable to that of the ambient gas of the intercore medium, taken to be 5000 cm$^{-3}$.

In summary, the four free parameters of the model are the dust emissivity index, $\beta$, the envelope temperature at the reference radius $r_0$, $T_0$, the envelope density at the reference radius $\rho_0$, and the density power-law index, $p$. The reference radius $r_0$ is arbitrary and has been taken as $r_0 = 1000$ AU.

With this model, we fitted the observed radial intensity profiles at 450 and 850 $\mu$m or 1.2 mm, and the observed SED from centimeter wavelengths up to 60 $\mu$m simultaneously. The uncertainty adopted for the intensity profiles was 20% at 850 $\mu$m and 50% at 1.2 mm and 450 $\mu$m (Di Francesco et al. 2008). The uncertainty of the flux densities used to build the SED was adopted to be 50%.

In order to compare the model with the observed intensity profile at each wavelength, we computed the intensity map from the model, and we convolved it with the beam, given as the sum of two circular Gaussians (the main and error beams). Finally, the circularly averaged profile was computed from the convolved map. We also simulated the effect of the finite chop throw used in the observations to cancel the sky emission. Thus, for each map position, we estimated the off-source intensity as the average intensity at a chop–throw distance of 120$''$ from the map (on-source) position, and we computed the difference between the on- and off-source intensities. From this, we computed the radial profile corrected for chopping.

In order to compare the model with the observed SED, for each data point with wavelength higher than 60 $\mu$m, we computed the model flux density by integration of the model intensity profile inside the reported aperture used for each measurement. In addition, for points with frequency below
Table 1
Best-fit Parameters to the Radial Profiles and SED of the Massive Dense Cores

| ID-Source     | D (kpc) | Lobs (L⊙) | Nmum | β | T0 (K) | ρ0 (g cm⁻³) | pb | χ rb | References |
|---------------|---------|-----------|------|---|--------|-------------|----|------|------------|
| 1-IC1396N     | 0.75    | 290       | 4    | 1.41 ± 0.19 | 43 ± 4 | (2.8 ± 0.4) x 10⁻¹⁷ | 1.62 ± 0.08 | 0.580 | 1.2 | 1 |
| 2-I22198      | 0.76    | 340       | 1.5  | 1.46 ± 0.31 | 43 ± 5 | (2.8 ± 1.0) x 10⁻¹⁷ | 2.45 ± 0.16 | 0.885 | ... | ... |
| 3-NGC 2071-IRS1 | 0.42   | 440       | 1    | 1.09 ± 0.21 | 40 ± 3 | (6.1 ± 1.0) x 10⁻¹⁷ | 1.83 ± 0.09 | 0.534 | ... | ... |
| 4-NGC 7129-FIRS2 | 1.25  | 460       | 1    | 1.55 ± 0.28 | 47 ± 4 | (5.9 ± 1.1) x 10⁻¹⁷ | 2.14 ± 0.11 | 0.454 | 1.4 | 1 |
| 5-CD2-3mn     | 2.50    | 700       | 2    | 1.42 ± 0.24 | 58 ± 7 | (7.4 ± 1.5) x 10⁻¹⁷ | 2.04 ± 0.10 | 0.552 | 2.2 | 1 |
| 6-I22172N-IRS1 | 2.40   | 830       | 3    | 1.49 ± 0.23 | 75 ± 10 | (3.7 ± 0.7) x 10⁻¹⁷ | 1.89 ± 0.08 | 0.283 | ... | ... |
| 7-OMC-1S      | 0.45    | 2000      | 1    | 1.42 ± 0.20 | 86 ± 9 | (8.8 ± 1.8) x 10⁻¹⁷ | 1.56 ± 0.10 | 0.319 | ?? | 2 |
| 8-AFGL 5142   | 1.80    | 2200      | 7    | 1.25 ± 0.20 | 70 ± 7 | (1.8 ± 0.2) x 10⁻¹⁶ | 2.00 ± 0.05 | 0.361 | ... | ... |
| 9-I05358+354N3 | 1.80   | 3100      | 1.48 | 1.28 ± 0.18 | 62 ± 6 | (6.4 ± 1.0) x 10⁻¹⁷ | 1.55 ± 0.05 | 0.229 | >0.8, 1.5 | 3, 7 |
| 10-I20126+4104 | 1.64  | 8900      | 8    | 1.82 ± 0.24 | 86 ± 9 | (8.4 ± 1.6) x 10⁻¹⁷ | 2.21 ± 0.11 | 0.607 | 1.6, 1.8, 2.2 | 3, 4, 5 |
| 11-I22134-IRS1 | 2.60   | 11800     | 3.5  | 1.70 ± 0.19 | 82 ± 8 | (3.1 ± 0.5) x 10⁻¹⁷ | 1.76 ± 0.06 | 0.477 | 1.3 | 3 |
| 12-HH80-81    | 1.70    | 2100      | 3    | 1.56 ± 0.14 | 108 ± 10 | (4.2 ± 0.6) x 10⁻¹⁷ | 1.78 ± 0.04 | 0.473 | ... | ... |
| 13-W3IRS5     | 1.95    | 140000    | 3.5  | 1.04 ± 12 | 260 ± 30 | (2.4 ± 0.3) x 10⁻¹⁷ | 1.46 ± 0.04 | 0.602 | 1.5, 1.4 | 4, 7 |
| 14-AFGL 2591  | 3.00    | 190000    | 1.5  | 0.96 ± 0.12 | 250 ± 20 | (5.4 ± 0.7) x 10⁻¹⁷ | 1.80 ± 0.03 | 0.549 | 1.0, 2.0, 1.0 | 4, 6, 7 |

Notes.

a Lobs taken from Palau et al. (2013). Nmum is the fragmentation level, taken from Palau et al. (2013) and assessed by estimating the number of millimeter sources within a field of view of 0.1 pc of diameter as detected with a millimeter interferometer with a mass sensitivity of ~0.3 M⊙ and a spatial resolution of ~1000 AU. For the four Cygnus X cores, Nmum has been revised with respect to the values given in Palau et al. (2013).

b Free parameter fitted by the model: β is the dust emissivity index, T0 and ρ0 are the temperature and density at the reference radius, 1000 AU; p is the density power-law index; χ r is the reduced χ as defined in Equation (6).

c Density power-law index from different works in the literature. References 1: Crimier et al. (2010); 2: Mezger et al. (1990); 3: Beuther et al. (2002); 4: van der Tak et al. (2000); 5: Shinnaga et al. (2008); 6: Mueller et al. (2002); 7: van der Tak et al. (2013). For I22134, the reported value is taken from Beuther et al. (2002) who fitted two power-law indices with a break at 32"; and we give here the outer power-law index. To convert from the reported intensity power-law index to the density power-law index, Beuther et al. (2002) adopt a temperature power-law index of 0.4. Similar for Shinnaga et al. (2008), for which the power-law break is taken at 12".

d Digitized data from Jenness et al. (1995).

e Sources for which only the radial intensity profile at 1.2 mm was fitted. For CygX-N63, Nmum was inferred from new Plateau de Bure observations in AB configuration (S. Bontemps 2013, private communication).

1000 GHz, we added the free–free emission of an unresolved source with a flux density extrapolated from the data points at centimeter wavelengths.

The fitting procedure was the sampling of the four-dimensional parameter space, using the same procedure as that described in Estalella et al. (2012) and Sánchez-Monge et al. (2013). For every set of parameters, we computed the residual χ²,

\[
χ² ≡ \sum_{i=1}^{n} \left( \frac{y_{i}^{\text{obs}} - y_{i}^{\text{mod}}(β, T0, ρ0, p)}{σ_i} \right)^2
\]

where the sum encompasses the points of the intensity profiles at 850 and 450 μm, and the points of the SED fitted by the model. The parameter space was searched for the minimum value of χ². For each source, the initial search ranges for the four parameters were β = 1.5 ± 1.5, T0 = 300 ± 300 K, ρ0 = (1.0 ± 1.0) x 10⁻¹⁶ g cm⁻³, and p = 1.5 ± 1.0. The search range was reduced a factor of 0.8 around the best-fit value of the parameters found for each loop, consisting in 2000 samples of the parameter space. The final best-fit values were taken after 10 loops. Once the best-fit parameters were found, their uncertainties were estimated through the increase in χ² (see Estalella et al. 2012; Sánchez-Monge et al. 2013). We assessed the quality of the fits through the value of the reduced chi-square,

\[
χ_r ≡ \sqrt{χ²_{\text{min}} / n - 4}
\]

In general, for all the sources, we found fits with χ_r ≃ 1, or even less, indicating that the errors of the data were slightly overestimated. In Figure 14 we show as example, the parameter space around the best-fit solution for the source IC 1396N.

3. RESULTS

Figures 2–5 present the best simultaneous fit to the 850 and 450 μm (or 1.2 mm) radial intensity profiles and the SED for the 19 massive dense cores. A summary of the fitted parameters is presented in Table 1. The four fitted parameters span a wide range of values. The dust emissivity index ranges from 1.0 to 1.9, with a mean value of 1.5. This is comparable to dust emissivity indices measured in high-mass envelopes (e.g., Mueller et al. 2002; Hill et al. 2006 for temperatures between 30 and 50 K), and corresponds to temperature power-law indices ranging from 0.34 to 0.40 (mean value: 0.37, consistent with Emerson 1988).

The fitted values for the temperature at 1000 AU range from 40 to 260 K, with a mean value of 83 K, and correlate with the
The temperature at 1000 AU and the bolometric luminosity correlate with a slope of \(0.24\), following approximately the Stephan–Boltzmann law (of slope +0.25, Table 1).

The range of densities at 1000 AU is \(10^{-3}\) to \(10^{-1}\) \(\text{cm}^{-3}\), with a mean value of \(-8 \times 10^{-7}\) \(\text{cm}^{-3}\). Finally, the radii where the temperature falls down to 10 K ranged from 0.2 to 18 pc, being the cores with higher temperature (at reference radius) where this radius is larger.

4. DISCUSSION

4.1. Comparison of Density Structure with Previous Works

We compared our inferred density power-law indices to the results of previous works where a similar methodology was applied for some of the cores of our sample. In the two last columns of Table 1, we list \(\beta_{\text{mod}}\), the density power-law index from the literature, together with the corresponding references. Crimier et al. (2010), van der Tak et al. (2000, 2013), and Mueller et al. (2002) fit one single power-law to the radial intensity profiles, being comparable to the work presented here, while Beuther et al. (2002) used two power-laws with a break at 32\(^{\circ}\). Within the regions fitted by the same authors, the tendency of flat and concentrated profiles is consistent with the results found in the present work (for example, IC1396N is flatter than NGC 7129-FIRS2 and CB3-mm as in Crimier et al. 2010; or DR21-OH (Mangum et al. 1992). \(\sigma_{\text{nth}}\) was estimated assuming a temperature of 20 K, \(\sigma_{\text{feedb}}\) is the non-thermal velocity dispersion for the studied core (thus including outflow feedback from the nascent protostars) from data in the literature (see Section 4.4 for references). \(\sigma_{\text{nth}}\) was estimated using the temperature at radius 0.05 pc as inferred from the modeled temperature profile (Tables 1 and 2). \(M_{\text{vir}}\) and \(\alpha_{\text{vir}}\) were assessed using the non-thermal velocity dispersion including feedback from outflows.

“Turbo. Mod.” refers to tentative turbulence mode according to works of the literature: “c” indicates that a detailed study has been done comparing the properties of the region with simulations or studying the probability density function; “c?” indicates that the only hints of possible compressive turbulence are that the region lies at the border of an expanding bubble/H\(\text{II}\) region. References for turbulence mode: 1: Beltrán et al. (2002b); 2: Schneider et al. (2013); 3: Sakai et al. (2013); 4: Liu et al. (2012); 5: López-Sepulcre et al. (2013); 6: Hunter et al. (1995); 7: Leurini et al. (2007); 8: Schneider et al. (2011); 9: Schneider et al. (2006).
yield differences of 0.2–0.4 in the density power-law index. The most important difference between previous works and this work is the way of determining the temperature profile. While Mueller et al. (2002), Crimier et al. (2010), and van der Tak et al. (2013) calculate the temperature profile self-consistently through radiative transfer codes, we assume that the temperature profile is related to the dust emissivity index (Section 2.2) and leave the temperature at a given radius as a free parameter. This is also different from Beuther et al. (2002), who assumed a fixed temperature power-law index of 0.4. In general, our method finds flatter temperature profiles compared to Crimier et al. (2010) and van der Tak et al. (2013), yielding higher density power-law indices. On the other hand, our method is perfectly consistent with the results of Mueller et al. (2002) for AFGL 2591. Therefore, once the different methodologies are taken into account, our methodology yields consistent results with previous works and allows to fairly compare the fitted parameters from one region to the other.

4.2. Uncertainty in the Fragmentation Level and Possible Biases in the Sample

Before comparing the inferred density structure for each massive dense core (estimated through the density power-law index \(p\)) to the fragmentation level (estimated through the \(N_{\text{mm}}\) parameter; see Table 1 and Palau et al. 2013), we discuss here the main uncertainties in the assessment of these properties and possible biases. First of all, we stress that the determination of both \(p\) and \(N_{\text{mm}}\) has been carried out applying the same methodology and criteria to all the cores and thus, although the absolute values might be subject to discussion, the relative value between the regions is meaningful and valid for a comparison. In particular, \(N_{\text{mm}}\) is a lower limit to the total number of fragments because of flux missed by the interferometers and because we are missing objects emitting at wavelengths different to millimeter. However, the sample presented in Palau et al. (2013) was selected applying strict criteria for the filtered emission and \(uv\)-coverage (see Column 8 of Table 3 of Palau et al. 2013), constraining this study to the most compact fragments (\(<5000\) AU). Since larger non-centrally peaked structures might be transient, this is not likely affecting our estimate of the fragmentation level. In addition, the number of infrared sources were compared to \(N_{\text{mm}}\), and were found to be correlated, indicating that \(N_{\text{mm}}\) is systematically underestimating the “real” fragmentation level of the core by only a factor of \(\sim 2\). Finally, Palau et al. (2013) also used radiation MHD simulations to show that \(N_{\text{mm}}\) is sensitive to the original fragmentation of the core. Altogether, this suggests that \(N_{\text{mm}}\) is already a good indicator of the fragmentation level if used to compare the different regions and not as an absolute value.

A possible bias could come from the different distances in the sample. However, for 16 out of 19 cores distances range only from 0.8 to 2.5 kpc, and no trend of \(N_{\text{mm}}\), \(p\), or any of the fitted parameters versus distance is found in our data (Table 1), indicating that this is not affecting our conclusions. Another bias could arise from different evolutionary stages of the cores of our sample, as simulations show that the degree of substructure in a cloud decreases with age (e.g., Smith et al. 2009). Our sample is not likely dramatically affected by this because the targets were selected to be in similar evolutionary stages: all targets harbor an intermediate-/high-mass protostar detected in the far-infrared, are associated with a strong and compact millimeter core, are associated with molecular outflows, and have not yet developed an (ultra-)compact H\(\text{II}\) region. The small differences in evolutionary stage of the cores of this sample were also studied in Palau et al. (2013) by estimating evolutionary indicators, and no relation between \(N_{\text{mm}}\) and these indicators was found (see, e.g., Figure 8(b) of Palau et al. 2013).

Therefore, no biases in distance, evolutionary stage, or missing fragments in \(N_{\text{mm}}\) should be strongly affecting the results presented in this work.

4.3. Trend of Fragmentation Level with Density Power-law Index and Density

In this section, we study the relation between the core parameters inferred from the model and the fragmentation level, quantified through the number of millimeter sources within a field of view of 0.1 pc (in diameter), \(N_{\text{mm}}\), as in Palau et al. (2013). We find no trend of \(\beta, T_0\), and total mass of the core with the fragmentation level (Tables 1 and 2). Conversely, Figure 6 presents the relation between the density power-law index \(p\), the central density (at 1000 AU) \(\rho_0\), and the density within a radius of 0.05 pc, \(n_{0.05\text{pc}}\), with the fragmentation level. Figure 6(a) reveals a possible weak trend of \(N_{\text{mm}}\) with the density power-law index, with low fragmentation levels found mainly in cores with steeper density profiles. Concerning \(N_{\text{mm}}\) versus \(\rho_0\), our sample splits up into two groups, cores with high fragmentation and high \(\rho_0\), and cores with lower fragmentation and low \(\rho_0\), suggesting that high central densities (in opposition to average density, as assessed in Palau et al. 2013) could be related to the fragmentation level. Finally, there is a clear trend of high fragmentation levels in cores with high \(n_{0.05\text{pc}}\) (Figure 6(c)). A closer inspection of the data using statistical tests, like the Spearman’s \(\rho\) and Kendall’s \(\tau\) rank correlation coefficients, indicates that \(N_{\text{mm}}\) and \(p\) show a faint anti-correlation (\(\rho \sim -0.49, \tau \sim -0.3\)), Pearson’s linear correlation coefficient \(R \sim -0.3\). As for \(n_{0.05\text{pc}}\), it is strongly correlated with \(N_{\text{mm}}\) (\(\rho \sim 0.70, \tau \sim 0.54\)), and the two parameters are well described by a linear relationship \((R \sim 0.90)\). These relations indicate that the high \(n_{0.05\text{pc}}\) likely arise in cores with rather flat \(p\) and also high \(\rho_0\).

A trend of high fragmentation level for flat density profiles was already suggested theoretically by Myhill & Kaula (1992). More recently, Girichidis et al. (2011) showed, by studying the evolution of collapsing non-magnetized turbulent massive cores for different initial density profiles, that cores with a flat density profile produce a high number of protostars, while concentrated density profiles rather yield one massive protostar in the core center. This can be understood in the framework of Jeans fragmentation, as the larger the density, the smaller the Jeans mass (for a given temperature), and the larger the number of expected fragments \(N_{\text{Jeans}}\). In Figure 6(c), we overplot the expected number of fragments estimated as \(N_{\text{Jeans}} = (M_{0.05\text{pc}} \times \text{CFE})/M_{\text{Jeans}}\), with \(M_{\text{Jeans}} = 0.6285 [T/10\text{K}]^{1/2} [n_{100}\text{pc}^{-3}]^{-1/2} M_\odot\), for which we used \(T \sim 20\text{ K}\), and \(M_{0.05\text{pc}}\) being the mass within a radius of 0.05 pc (calculated directly from the density law inferred from our model). The core formation efficiency (CFE) was adopted to be 17\%, the average of the CFEs measured in Palau et al. (2013). Thus, the trend of higher fragmentation for higher densities within a radius of 0.05 pc is consistent with what is expected for Jeans fragmentation. The relation found in this work between fragmentation level (which could be regarded as a proxy to cluster richness) and gas density is reminiscent of the relation found on larger spatial scales between cluster mass or protostellar density and gas surface density (e.g., González-Lópezlira et al. 2012; Lombardi et al. 2013; Pflaum-Altenburg et al. 2013).
In the last panel, the Jeans number is calculated as $\frac{M_{\text{core}}}{\rho \mu}$ (see Table 2 and Section 4.2), and further studies should be conducted in this direction.

### 4.4. Physical Processes Affecting the Density Structure of Massive Dense Cores

With the aim of shedding light on which physical conditions promote fragmentation in massive dense cores, in this section, we study whether there is any relation between different physical processes and the density structure (density profile and central density) of massive dense cores.

**Time Evolution.** It has been shown both from observations and numerical simulations that structures within collapsing molecular clouds become more centrally peaked with time (e.g., Smith et al. 2009; Giannetti et al. 2013). Therefore, the cores for which we measure higher values in the density power-law index $p$ could just correspond to the most evolved ones. However, we searched for any relation between $p$ and the ratio of the bolometric luminosity to the single-dish mass parameter (an evolutionary indicator used in Palau et al. 201318), and found no trend in our data (Figure 7(a)). This lack of correlation of $p$ with time probably results from the fact that our sample consists of cores at very similar evolutionary stages (Section 4.2), not properly sampling broad enough timescales, and suggests that other processes in addition to time evolution are probably also playing a role in determining the density structure of a dense core.

**Rotational-to-gravitational Energy ($\beta_{\text{rot}}$).** The rotation of a massive dense core is expected to promote flattening of its density profile. In order to test this in our sample, we completed the values of rotational-to-gravitational energy ratios already estimated in Palau et al. (2013) with the value for the core added in this work (DR21-OH), observed by Girart et al. (2013) with similar conditions of sensitivity and spatial resolution as the sample of Palau et al. (2013). Here, we estimated $\beta_{\text{rot}}$ for DR21-OH following exactly the same method as in Palau et al. (2013), i.e., using NH$_3$(1,1) data (Mangum et al. 1992), and obtained a value of 0.24. We also estimated $\beta_{\text{rot}}$ for OMC-1S from the NH$_3$(1,1) data by Wiseman & Ho (1998). It is worth mentioning that these measurements of $\beta_{\text{rot}}$ must be regarded with caution as the velocity gradients observed might not be necessarily associated with rotation but could arise from multiple velocity components or infall motions (e.g., Lee et al. 2013). Keeping this in mind, in Figure 7(b) we present the relation between $\beta_{\text{rot}}$ and $p$, showing a weak inverse trend. This suggests that the initial angular momentum alone might not be the only agent shaping the density profile of a core. We also present an updated version of the plot of $N_{\text{mm}}$ vs $\beta_{\text{rot}}$ (after Palau et al. 2013) including these new measurements, and the updated plot, shown in Figure 8, indicates a possible trend of $\beta_{\text{rot}}$ with fragmentation level, which deserves further studies.

**Non-thermal Velocity Dispersion ($\sigma_{\text{nth}}$).** Palau et al. (2013) estimate the non-thermal velocity dispersion from the linewidth measured in NH$_3$(1,1) of a quiescent massive dense core in the immediate surroundings of the core where fragmentation was assessed. This can be regarded as a first approach to the initial turbulent dispersion. We completed the values of non-thermal “initial” velocity dispersions by adding two new measurements (CygX-N48 and DR21-OH by Mangum et al. 1992, Table 2). However, the non-thermal velocity dispersions cover a small range of values, from 0.33 to 0.67 km s$^{-1}$, and did not show any relation with the fragmentation level. We additionally study the relation of non-thermal velocity dispersion of the fragmenting cores (thus including feedback from outflows), covering a broader range from 0.41 to 2.16 km s$^{-1}$, with the density profile (Table 2, where we used the values from NH$_3$(1,1) observed with the Very Large Array, VLA; Torrelles et al. 1989; Zhou et al. 1990; Mangum et al. 1992; Tieftrunk et al. 1998; Wiseman & Ho

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18 For DR21-OH we estimated a ratio of bolometric luminosity to single-dish mass of 27.8.
Figure 7. (a) Relation between the bolometric luminosity to the single-dish mass parameter $L_{\text{bol}}/M_{\text{sd}}$ and the density power-law index. (b) Relation between rotational-to-gravitational energy $\beta_{\text{rot}}$ and the density power-law index. (c) Relation between non-thermal velocity dispersion (including outflow feedback) and density power-law index. Panels (b) and (c) include new cores after Palau et al. (2013, see Section 4.4). In all panels, red dots correspond to cores with “confirmed” compressive turbulence or with hints of compressive turbulence, and blue dots correspond to cores with no assessment of the turbulence mode in the literature (see Table 2 and Section 4.4).

Figure 8. Relation between fragmentation level $N_{\text{mm}}$ and the rotational-to-gravitational energy ratio, after Palau et al. (2013, i.e., including new measurements for OMC-1S and DR21-OH). Red dots correspond to cores with “confirmed” compressive turbulence or with hints of compressive turbulence, and blue dots correspond to cores with no assessment of the turbulence mode in the literature (see Table 2 and Section 4.4).

(A color version of this figure is available in the online journal.)

1998; Gómez et al. 2003; Sánchez-Monge et al. 2013). Since no clear trend is found (see Figure 7(c) and Table 2), this indicates that the density profile and the turbulent velocity dispersion are probably independent quantities. Finally, we estimated the virial masses and virial parameter ($M_\text{vir}/M_\text{0.05pc}$) using the non-thermal velocity dispersions of the fragmenting cores (i.e., including feedback) and found no relation of these quantities with the density power-law index or the fragmentation level.

**Turbulence Mode: Compressive versus Solenoidal.** In order to study if different turbulence modes could be affecting the density structure of massive dense cores, we searched the literature for any evidence of our massive dense cores being affected by expanding shells/bubbles created by nearby O-type stars, and our findings and references are listed in the two last columns of Table 2. Regions with hints in the literature of being associated with expanding shells or H II regions, such as bright-rimmed clouds, etc., or located at the meeting point of converging flows, are classified as “possible compressive,” while regions for which the probability density function has been found to be consistent with compressive turbulence are classified as “confirmed compressive.” Both “possible” and “confirmed” compressive-turbulent cores (see Table 2 to distinguish among both types) are assigned a “red” color in the figures, while the “blue” color corresponds to cores where the turbulence mode cannot be assessed with the current information (thus a solenoidal mode cannot be ruled out for “blue” cores). Figure 6 shows that “compressive-turbulent” cores tend to have large $N_{\text{mm}}$ and cover a wide range of density power-law indices (from 1.5 to 2). In addition, cores with $n_0 > 10^{-16}$ g cm$^{-3}$ and $n_{0.05pc} > 6 \times 10^5$ cm$^{-3}$ fall all within the “compressive-turbulent” group (see Figures 6(b) and (c)). This could be consistent with compressive turbulence because this mode yields higher density contrast structures than the solenoidal mode (e.g., Federrath et al. 2008, 2010). Recently, Tremblin et al. (2014) found that expanding H II regions or bubbles tend to induce steep density profiles in the cores at the bubble edges. Thus, the steep density profiles obtained in DR21-OH, AFGL 5142, and CB3 ($p \sim 2$) could have been produced by the expanding ionization fronts from the massive stars near these regions (Hunter et al. 1995; Schneider et al. 2011; Sakai et al. 2013). A more detailed and uniform study of the turbulence mode in each core would be required to definitely assess the role of the different turbulence modes in setting the density structure of massive dense cores.

**Magnetic Field.** Magnetic field could affect the density structure of a core because it helps removing angular momentum, yielding rather steep density profiles. We tested this by using the magnetohydrodynamic simulations from Commerçon et al. (2011) of strongly ($\mu = 2$, with $\mu$ being the mass-to-flux over the critical mass-to-flux ratio) and weakly ($\mu = 130$) magnetized cores. These simulations were found to reproduce our data remarkably well (Palau et al. 2013). It is important to note that in these simulations, the initial density profile is the same and rather flat for both the $\mu = 2$ and $\mu = 130$ cases. We extracted
the density profiles of Commerçon et al. (2011) simulations for \( \mu = 2 \) and \( \mu = 130 \) cases, by making an average of the density on concentric spherical shells weighted by the mass for each cell in the shell. The result is displayed in Figure 9, and shows that the \( \mu = 2 \) case evolved into a more concentrated profile than the \( \mu = 130 \) case, for radii up to \( \sim 0.05 \) pc or \( 10,000 \) AU. This result is consistent with the fact that for the low magnetic field case (\( \mu = 130 \)), the fragmented area is larger because of conservation of angular momentum, which gives a flatter density distribution at the center. And the opposite, strong magnetic braking (in the \( \mu = 2 \) case) helps concentrate matter in the center and gives a steeper profile. In addition, previous theoretical work including ambipolar diffusion (e.g., Lizano & Shu 1989) also predict steep density profiles (density power-law indices of \( \sim 2 \)). Thus, the current theoretical and numerical works suggest a relation between the density power-law index of massive dense cores and the magnetic field properties. Finally, we also used the simulations from Commerçon et al. (2011) to estimate the density within a radius of \( 0.05 \) pc for both \( \mu = 2 \) and \( \mu = 130 \), and find \( n_{0.05 \text{pc}} \sim 2.3 \times 10^5 \) cm\(^{-3} \) and \( 5.8 \times 10^5 \) cm\(^{-3} \), respectively. This, together with the number of millimeter sources that a typical interferometer would detect in each simulation (estimated in Palau et al. 2013), allowed us to compare the results of these simulations to our \( N_{\text{mm}} \) versus \( n_{0.05 \text{pc}} \) plot showing observational data (see Figure 6(c)). The values predicted by the simulations match the trend seen in the observational data remarkably well, suggesting that the magnetic field strength might be related to \( n_{0.05 \text{pc}} \) of massive dense cores, with small densities found in the strongly magnetized cores and large densities found in weakly magnetized cores. Overall, the agreement between Commerçon et al. (2011) simulations and our data is very good and suggests that magnetic field might be affecting the shape and density of massive dense cores, which in turn seems to be related to the fragmentation level.

5. CONCLUSIONS

In order to study the relation between the density profile of massive dense cores and the fragmentation level, we have fitted simultaneously the radial intensity profiles at 450 and 850 \( \mu \)m and the SED of 19 massive dense cores for which their relative fragmentation level was known from previous works. Although the parameter used to estimate the fragmentation level is a lower limit, its relative value for the different cores is significant because it is assessed in a uniform way for all of them. The sample consists of massive dense cores undergoing active star formation and being at similar evolutionary stages. We modeled the cores as spherical envelopes with density and temperature decreasing with radius following power laws and found a weak trend of lower fragmentation for cores with steeper (\( p \gtrsim 2.0 \)) density profiles. A correlation is found between the fragmentation level and the density within a radius of 0.05 pc (the radius where fragmentation was assessed), suggesting that high fragmentation levels might be related with flat cores and cores with high central densities. This correlation is consistent with Jeans fragmentation, as high densities yield lower Jeans masses.

While we find no clear relation between velocity gradients or velocity dispersion and the density power-law index of our massive dense cores, cores with compressive turbulence seem to be associated with high central densities, thus promoting fragmentation. On the other hand, a comparison with radiation magneto-hydrodynamical simulations suggests that a strong magnetic field could help shape steep density profiles in massive dense cores, for which low fragmentation levels are found. Thus, it is of crucial importance to study the relation of density profile, turbulence mode, and magnetic field from both an observational and numerical point of view.

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APPENDIX

SINGLE-DISH AND INTERFEROMETRIC IMAGES

Figures 10–13 show the 450 and 850 \( \mu \)m (or 1.2 mm) single-dish emission of each massive dense core (from Motte et al. 2007; Di Francesco et al. 2008) along with the high angular resolution millimeter interferometric maps already presented and studied by Bontemps et al. (2010) and Palau et al. (2013). The single-dish data, together with the Spectral Energy Distribution for each core, allowed us to infer the density structure, which we relate in this paper with the fragmentation level in each massive dense core.
Figure 10. Left and central panels: JCMT/SCUBA 850 and 450 μm emission (Jenness et al. 1995; Di Francesco et al. 2008). For each source, the two green squares are ~0.1 × 0.1 pc², the size of the mm interferometer map (right panel; Palau et al. 2013) revealing the fragmentation in each core. For IC1396N, NGC 7129-FIRS2, and CB3-mm, contours of 850 (450) μm emission (left (middle) panels) are 8%–99%, increasing in steps of 10% of the peak value, 5.0 (25.3), 4.1 (48.9), and 2.1 (12.8) Jy beam⁻¹, respectively. For I22198, contours of 850 (450) μm emission (left (middle) panel) are 20%–99%, increasing in steps of 20% of the peak value, 5.5 (9.8) Jy beam⁻¹. For NGC 2071, contours of 850 (450) μm emission (left (middle) panel) are 5%–99%, increasing in steps of 10% of the peak value, 13.1 (97.3) Jy beam⁻¹. Contours for interferometric images (right panels) are −4, 4, 8, 16, 32, and 64 times the rms noise of each map as given in Palau et al. (2013). (A color version of this figure is available in the online journal.)
Figure 11. Left and central panels: JCMT/SCUBA 850 and 450 μm emission (Di Francesco et al. 2008). For each source, the two green squares are \( \sim 0.1 \times 0.1 \) pc\(^2\), the size of the mm interferometer map (right panel; Palau et al. 2013) revealing the fragmentation in each core. For I22172N, OMC-1S, AFGL 5142, I05358NE, and I20126, contours of 850 (450) μm emission (left (middle) panels) are 8%–99%, increasing in steps of 10% of the peak value, 2.0 (13.2), 73.5 (390), 9.5 (45.4), 7.9 (27.6), 6.1 (62.4) Jy beam\(^{-1}\), respectively. Contours for interferometric images (right panels) are \(-4, 4, 8, 16, 32, \) and 64 times the rms noise of each map as given in Palau et al. (2013).

(A color version of this figure is available in the online journal.)
Figure 12. Left and central panels: JCMT/SCUBA 850 and 450 μm emission (Di Francesco et al. 2008). For each source, the two green squares are \( \sim 0.1 \times 0.1 \text{ pc}^2 \), the size of the mm interferometer map (right panel; Palau et al. 2013) revealing the fragmentation in each core. For I22134, HH80, W3IRS5, and AFGL 2591, contours of 850 (450) μm emission (left (middle) panels) are 8%–99%, increasing in steps of 10% of the peak value, 2.6 (20.4), 8.3 (62.1), 18.0 (76.8), 7.9 (71.4) Jy beam\(^{-1}\), respectively. Contours for interferometric images (right panels) are \(-4, 4, 8, 16, 32, 64, \text{ and } 128\) times the rms noise of each map as given in Palau et al. (2013).

(A color version of this figure is available in the online journal.)
Figure 13. Left and central panels: JCMT/SCUBA 850 μm (or IRAM 30m 1.2 mm) and 450 μm emission (Motte et al. 2007; Di Francesco et al. 2008). For each source, the two green squares are $\sim 0.1 \times 0.1$ pc$^2$, the size of the mm interferometer map (right panel, Bontemps et al. 2010, Girart et al. 2013) revealing the fragmentation in each core. For CygX-N53, CygX-N48 and DR21-OH, contours of 850 (450) μm emission (left (middle) panels) are 8%–99%, increasing in steps of 10% of the peak value, 7.1 (38.9), 16.3 (91.8), 33.4 (215) Jy beam$^{-1}$, respectively. For CygX-N12, and CygX-N63, contours of 1.2 mm emission (left panels) are 8%–99%, increasing in steps of 10% of the peak value, 1.0, 0.9 Jy beam$^{-1}$, respectively. Contours for interferometric images of CygX-N53, CygX-N12, and CygX-N63 (right panels) are $-4, 4, 8, 16, and 32$ times the rms noise of the 1.2 mm map, 1.9, 1.9, and 4.2 mJy beam$^{-1}$, respectively (Bontemps et al. 2010). Contours for the interferometric image of CygX-N48 (right panel) are $-4, 4, 8, 12, 16, 20, 24, 28, and 32$ times the rms noise of the 0.88 mm map, 5 mJy beam$^{-1}$ (Girart et al. 2013).

(A color version of this figure is available in the online journal.)
A.1. Example of Reduced Chi-square Fit

We present the parameter space around the best fit solution of the envelope model (Section 2.2) for source IC 1396N. The four free parameters (dust emissivity index $\beta$, envelope temperature at the reference radius $T_0$, envelope density at the reference radius $\rho_0$, and density power-law index $p$, or $q_d$) are reasonably well constrained when all pairs of parameters are considered (Figure 14).

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