HEMATOLOGY | RESEARCH ARTICLE

Red blood cell size differential method for time-series detailed monitoring of anemic disorders with RBC size abnormalities in mean corpuscular volume (MCV) and/or red blood cell distribution width (RDW)

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Abstract: Background: Size heterogeneity in red blood cells (RBCs), as indicated by elevated RBC distribution width (RDW), is increasingly considered a prognostic factor in various diseases. However, the semi-quantitative nature of the RDW value appears limited when evaluating quantitative changes in time-series RBC size distributions over a clinical course. Methods: We developed a time-series anemia monitoring program by displaying progressive differences between six size fractions in an RBC size distribution. To standardize each variation precisely, our program includes an angular transformation that is applied to all measured count ratio data. Results: By representing microcytic and/or macrocytic changes in time series independently, this method appears to improve evaluations of anisocytosis, reflecting the responsiveness of treatments and effects, such as deficiencies in iron or vitamin B12. Time-series displays of RBC size changes also appear to enable verification of latent clinical developments at earlier stages and the characterization of imbalances between RBC supply and RBC loss in anemic pathologies. Conclusions: By displaying linear relationships between RBC size categories on a time scale, our proposed...
monitoring method quantifies potentially applicable pathological information. This mode of representation appears to offer details about high RDW values and latent adverse outcomes related to anemic pathogenesis.

Subjects: Computer Graphics & Visualization; Hematology; Medical Statistics & Computing

Keywords: anemia monitoring; flow cytometry; measurement uncertainty; MCV; RDW

1. Introduction

In a complete blood cell count (CBC), performed as a routine laboratory test in anemia diagnosis, a hematology analyzer measures the volume of each erythrocyte to create a histogram of cell size distribution. This probability distribution provides two main output parameters: the mean corpuscular volume (MCV), which is the mean value of the distribution, and the red blood cell distribution width (RDW), which represents the degree of dispersion in the distribution (Kachel, 1982; Tatsumi et al., 1999). Recently, elevated RDW has been investigated as a predictor of mortality in various non-hematological disorders, such as inflammation and circulatory diseases (Cauthen, Tong, Jain, & Tang, 2012; Hu et al., 2013; Lippi & Plebani, 2014; Montagnana, Cervellin, Meschi, & Lippi, 2012). However, when interpreting central values, such as MCV and RDW, in time series, it can be difficult to evaluate information about cellular volume changes with minimal or latent anisocytosis in the red blood cell (RBC) size distribution.

Accordingly, we established a new evaluation method called “RBC size differentials”, which enables time-series partial analysis of RBC size distribution derived from a hematology analyzer without additional cost. Using data from daily control checks for counting RBCs and white blood cells (WBCs), we investigated the measurement uncertainty of our flow cytometric approach and verified the reliability of our computed indices obtained from RBC size differential methods.

2. Methods

2.1. Data collection

To examine CBC data, including MCV and RDW indices, we used an XE-5000 hematology analyzer (a recent model; Sysmex Corp., Kobe, Japan) at Sasebo City General Hospital from June 2013 to May 2016 and an SF-3000 (a past model; Sysmex Corp., Kobe, Japan) at Nagasaki Harbor Medical Center Community Hospital from July 1998 to September 2005 for a pilot study. This study’s data were acquired through standard blood test procedures with daily quality control checks. Data from 307,246 clinical samples data from the XE-5000 analyzer and 5,087 clinical samples from the SF-3000 analyzer were registered in our database for RBC size differentials.

To obtain the probability distributions of RBC size, PNG-format digital images were first output from the XE-5000 analyzer. Next, the images were converted to numerical form by subdividing the x-axis into 256 points for compilation in a relational database. Alignment of the x-axis relative to the origin was confirmed by statistically comparing the cumulative mean value of RBC size to the cumulative analyzer’s MCV data (for details, see Appendix 1 and Figure A1). Using the same approach, the printed image data of RBC size distributions from the SF-3000 analyzer were manually digitized in another database. When comparing MCV values for a single given probability distribution, values from relational databases were observed to be consistent with MCV values from the hematology analyzer output.

2.2. RBC size differential method

2.2.1. Establishing six RBC size fractions (Step 1)

Ranging between extreme limits of 41–160 fL, RBC size distributions were fractionized into the following six size fractions every 20 fL, called “RBC size differentials”, as shown in the RBC size
distribution in Figure 1: under-microcytic (uMic), microcytic (Mic), normocytic (Nor), macrocytic (Mac), megalocytic (Meg), and over-megalocytic (oMeg).

2.2.2. Computing the count ratio \( p \) of each RBC size fraction (Step 2)
Using the relational database, we computed the count ratio \( p \) as the percentage of each fraction's area under the curve within the 41–160 fl RBC size distribution. The six count ratios' values of \( p \) corresponding to each of the respective fractions were labeled \( %uMic \), \( %Mic \), \( %Nor \), \( %Mac \), \( %Meg \), and \( %oMeg \).

2.2.3. Transforming the count ratio \( p \) variable to angle ratio \( \theta \) to standardize precision (Step 3)
Because our method for representing true change requires the calculation of differences, variations in precision among the six fractions must be standardized. Subjecting the count ratio \( p \) data to a variance-stabilizing transformation (Kirk, 2013) resulted in distributions with a standard deviation (SD) value independent of the \( p \) variable. This angular transformation is a function defined as \( \theta(p) = 2 \cdot \arcsin\sqrt{p} \), which we called Angit(p). The mean values of the transformed six angle ratios \( \theta \)s are then subtracted from one another, thus reducing disparities in precision. Corresponding to the fractions identified in Step 2, the angle ratios \( \theta \)s were called \( \theta_uMic \), \( \theta_Mic \), \( \theta_Nor \), \( \theta_Mac \), \( \theta_Meg \), and \( \theta_oMeg \).
2.2.4. Establishing RBC size differential indices (Step 4)

The six angle ratio $\theta$s were utilized alone as each RBC size differential index, with equal precision in theory. Furthermore, two additional RBC size differential indices were established by subtracting the $\theta_{\text{Nor}}$ value from the $\theta_{\text{Mic}}$ and $\theta_{\text{Mac}}$ values. Respectively called $[\theta_{\text{Mic}}-\theta_{\text{Nor}}]$ and $[\theta_{\text{Mac}}-\theta_{\text{Nor}}]$ with equal precision in theory (Taylor, 1997), these indices reflect the difference in each RBC size fraction relative to the central Nor-fraction.

2.3. Measurement uncertainty in flow cytometric count data for blood cell differentials

We evaluated measurement uncertainty in our blood cell differential method with data from daily quality control checks based on the notion that the fluctuation in repeated measurements of the same sample should reflect the measurement uncertainty.

We compared the differences in the uncertainty in differential indices between the RBC size differentials and WBC differentials. Using statistical analyses with 38 courses of two different series of quality control checks with different cell concentrations by the XE-5000 analyzer, we investigated the uncertainty-stabilizing effects of both angular transformation and Logit transformation on both the count ratio index and the subtraction index, according to the degree of the fluctuation’s dispersion based on each index’s SD, which is closely reflective of precision in general. The additional coefficient of variation of these SD values, which we called “SD dispersion”, was calculated as (standard deviation of SD values/mean of SD values) × 100. For our rationale for applying the Angit(p) and Logit(p) functions, see Appendices 2 and 3.

2.4. Cut-off values of RBC size differential indices evaluated by receiver operating characteristic (ROC) curve analysis

Reference intervals of MCV and RDW were determined by satisfying the following clinically accepted criteria for normal RBC volume conditions: (1) an MCV from 80 to 100 fl (or 10-15L) (Sacher, McPherson, & Campos, 1991); and (2) an RDW-CV < 16%. RDW-CV was calculated as (standard deviation of mean corpuscular volume/mean corpuscular volume) × 100. A cut-off of 16% was identified as the upper limit of a normal sample (Rezende, Lijfering, Rosendaal, & Cannegieter, 2014). We evaluated the count ratio indices of $\theta_{\text{Mic}}$, $\theta_{\text{Mic}}$ and $\theta_{\text{Mac}}$ and the subtraction indices of $[\theta_{\text{Mic}}-\theta_{\text{Nor}}]$ and $[\theta_{\text{Mac}}-\theta_{\text{Nor}}]$ as the discriminators for RBC size abnormality according to the clinical criteria for MCV and RDW values: normocytosis (80 $\leq$ MCV $\leq$ 100 and RDW-CV < 16%), microcytosis (MCV < 80 fl), macrocytosis (MCV > 100 fl) and normal range of RDW (RDW-CV < 16%). We determined the optimal cut-off values based on the method using the Youden index by ROC analysis (Hajian-Tilaki, 2013) with 307,246 CBC samples from the XE-5000 analyzer and 5,087 samples of patients with hematological disorders from the SF-3000 analyzer. Then, we compared the cut-off points between the two hematology analyzers: a recent model and past model manufactured prior to sheath-flow method integration (Tatsumi et al., 1999). ROC analysis was performed by statistical computing, using R software via http://www.R-project.org (The R Project for Statistical Computing, Vienna, Austria).

2.5. Graph preparation for visualizing the changes in time-series CBC data

The clinical courses of all anemic patients with RBC size abnormalities or RDW elevation were evaluated using our CBC time-series graph preparation program. For Cases 1–5, we compared similarities and differences in graph patterns among patients of differing pathologies by means of RBC size differentials, superimposed RBC size distributions and other CBC data while considering hidden measurement uncertainty in RBC size differential indices. All numerical computations and graphs for this study were conducted using Microsoft Excel software.
2.6. Ethics
This study was approved by the Institutional Review Board of Nagasaki Harbor Medical Center Community Hospital and Sasebo City General Hospital and was conducted in accordance with the ethical principles of the Declaration of Helsinki. Its communication is consistent with the Code of Ethics of the American Medical Writers Association.

3. Results

3.1. Characteristics of measurement uncertainty in blood cell differential methods (Figure 1 and Table 1)
Figure 1 shows the fluctuation patterns of measurement uncertainty in each differential index: (1) Count ratio index and (2) Subtraction index in both methods of (A) RBC size differentials and (B) WBC differentials. Non-transformed differential indices are shown in the graphs at left (a-series), transformed indices by Angit function in the middle graphs (b-series), and transformed indices by Logit function in the graphs at right (c-series). The statistical values of mean ± standard deviation in each index are noted at the positions of the corresponding lines, and computed SD dispersions (CV%) are noted at the bottom of each graph. All SD values and SD dispersion values from the total of 76 courses of quality control checks are analyzed statistically in Table 1.

First, the angular transformation by Angit function standardized the uncertainty most effectively in the count ratio index, according to the smallest SD dispersion; however, the uncertainty in the subtraction index exhibited an obvious discrepancy between RBC size differentials and WBC differentials. Next, there were typical graphical findings of synchronized patterns in the fluctuations in the count ratio index, revealing both reciprocal mirror and parallel images between side-by-side fractions, which caused the amplification and offset of fluctuation in the subtraction index only in RBC size differentials. Because the statistical comparison of SD values in the transformed count ratio index by Angit function revealed no difference between RBC size differentials vs. WBC differentials (A-1-b vs. B-1-b in Figure 1 and Table 1), we speculated that this discrepancy in the subtraction index might be caused by uncertainty other than precision, which was already equalized in the count ratio index.

3.2. Cut-off points of each RBC size differential index (Table 2)
ROC analysis indicated that for both hematology analyzers, $\theta_{\text{Nor}}, \theta_{\text{Mic}}$ and $\theta_{\text{Mac}}$ might be good discriminators of normocytosis, microcytosis and macrocytosis, respectively. Furthermore, because the cut-off point of the $[\theta_{\text{Mic}}-\theta_{\text{Nor}}]$ index was exactly 0.00π for both analyzers, microcytosis of MCV < 80 fL might correspond to the same distributions as the microcytic state of $[\theta_{\text{Mic}}-\theta_{\text{Nor}}] > 0$ for both analyzers. By contrast, for judgment of the macrocytic state, the cut-off point of the $[\theta_{\text{Mac}}-\theta_{\text{Nor}}]$ index was −0.02π for the XE-5000 analyzer and −0.05π for the SF-3000 analyzer. These different shifts in cut-off point from 0.00π might depend on their skewness to the left in the RBC size distributions based on the mechanical difference in analyzers with or without sheath-flow methods (Tatsumi et al., 1999). However, the $[\theta_{\text{Mic}}-\theta_{\text{Nor}}]$ and $[\theta_{\text{Mac}}-\theta_{\text{Nor}}]$ indices might be good indicators of hematological microcytosis and macrocytosis, respectively, based on their high AUC% values.

3.3. How this method facilitates the visualization of states of size abnormality: Displaying multi-variable time series
Figures 2–4 show how the RBC volume differential time series might complement MCV and RDW indicators to improve the pathological diagnosis of various anemic disorders. The x-axis in days is common to all time-series graphs, and the following indices are represented by the y-axes in the four time-series partitions from top to bottom: (1) hemoglobin (HGB) on the main y-axis and hematocrit (HCT) on the second y-axis; (2) MCV on the main y-axis and RDW-CV% on the second y-axis; (3) angle ratio $\vartheta$ (π) on the main y-axis (linear scale) and its original count ratio p (%) on the second y-axis (non-linear scale); and (4) RBC size indices. At the bottom, the superimposed RBC size distributions from the analyzer indicate partial qualitative changes (labeled “Frequency” for “Frequency distribution graph”). All the following cases appear to indicate relative RBC size fractional changes for specific time periods according to varying pathologies.
3.4. Assessing time-series RBC size changes associated with erythroid maturation disorders (Figure 2)

In Case 1, before vs. after TS-1 chemotherapy for a lung cancer patient (typical case), and in Case 2, before vs. after an allogeneic bone marrow transplant with RBC transfusions for a severe aplastic anemia patient

In Case 1, there were a few spikes in the [θMac−θNor] line (marked with arrows) in accordance with drip infusion therapies, which might have been deviations due to possible unexpected uncertainty propagation. Although the megalocytic fraction was stable after chemotherapies with CBDCA, PTX and BV, the increasing megalocytic trend with a complementary normocytic decrease immediately before Day 257 suggested DNA synthesis inhibitor effects due to disruption of erythroid maturation by TS-1.

In Case 2, two time points of macrocytic states with high-level megalocytic fractions seemingly derived from pathological erythroid clones with maturation disorder gradually disappear due to conditioning regimens, and the prominent microcytic increase might reflect RBC supply from transfusions. After Day 89, normocytic and macrocytic increases without a macrocytic state appear to indicate normal erythroid recovery derived from transplanted stem cells, and the concurrent microcytic decrease suggests rapid removal of older transfused RBCs from the peripheral blood.

3.5. Assessing time-series RBC size distributions for pathological abnormalities related to disseminated intravascular coagulation (DIC), with potentially shortened RBC lifespan (Figure 3)

In Case 3, caused by massive vascular bleeding, and in Case 4, caused by extravascular hemolysis with findings of RBC fragmentation.

In Case 3, the increase and subsequent decrease in the megalocytic fraction mirror the decrease and subsequent increase in the normocytic fraction; these transitions appear to reflect marrow responses to severe anemia caused by bleeding. Case 4 offers an interesting comparison because the normocytic and macrocytic increases appear to reflect marrow responses to severe anemia caused by hemolysis with RBC fragmentation, as indicated by the leftward shift of the frequency distribution graph. In both cases, the transient megalocytic increase might be a similar basic pattern of reaction to severe anemia, except for the brief presence of a microcytic state in Case 4.

3.6. Assessing changing microcytic states caused by iron deficiency in different clinical backgrounds (Figure 4)

In Case 5, showing a typical recovery course with ferric therapy, in contrast to Case 6, showing retardation in anemia recovery due to massive menstrual bleeding for one week, and Case 7, showing the common complication of iron deficiency during vitamin B12 treatment.

Cases 5 and 6 both exhibited a decreasing [θMic−θNor] line and similar durations of a microcytic state (θMic > θNor). However, only Case 6 exhibited an additional macrocytic increase with a macrocytic state (θMac + 0.05π > θNor) and a bimodal pattern in the RBC volume distribution, which might be a transient response of excessive erythropoiesis to massive bleeding. In Case 7, concurrent with a decreasing [θMac−θNor] and θMeg, an upward trend in the [θMic−θNor] line and a subsequent microcytic state were observed. Because this [θMic−θNor] index increase appears to indicate the extent of iron deficiency, this time-series may help guide the timing or decision for ferric medicine treatment—specifically, one week earlier than conducted for Case 7.

3.7. Assessing fractional rebalancing between RBC supply and RBC loss (Figures 2 and 3)

In our view, RBC size differential methods in time series have the potential to quantify each fraction’s change rates in the RBC size distribution. Although the superimposed RBC size distributions of Cases 1 and 3 merely present similar increases in the megalocytic fraction, the RBC size differentials
Table 1. Statistics for the evaluation of measurement uncertainty in flow cytometric differential data

(a) RBC size differentials of quality control samples

| RBC size differential index | Checks with QC****0810 series (n = 38) | Checks with QC****0811 series (n = 38) |
|----------------------------|----------------------------------------|----------------------------------------|
|                            | RBC count: (234 ± 2)×10^4/μL MCV: 76.5 ± 1.9 fl RDW-CV: 16.2 ± 1.0% | RBC count: (441 ± 3)×10^4/μL MCV: 83.1 ± 1.2 fl RDW-CV: 14.5 ± 0.3% |
|                            | SD value | SD dispersion | SD value | SD dispersion |
|                            | Mean ±SD  | Mean (%) ±SD (%) | Mean ±SD | Mean (%) ±SD (%) |
| 1. Count ratio index       |          |               |          |               |
| a %Mic                    | 0.9% ±0.3% | 64* ±11 | 1.5% ±0.4% | 41* ±3 |
| %Nor                     | 1.3% ±0.3% |           | 1.1% ±0.3% |           |
| %Mac                     | 0.3% ±0.1% |           | 0.7% ±0.2% |           |
| b Angit(Mic):%Mic         | 0.006π ±0.002π | 37* ±15 | 0.010π ±0.003π | 22* ±4 |
| Angit(Nor):%Nor           | 0.009π ±0.002π |           | 0.007π ±0.002π |           |
| Angit(Mac):%Mac           | 0.005π ±0.001π |           | 0.008π ±0.002π |           |
| c Logit(Neu)              | 0.038 ±0.014 | 39 ±13 | 0.066 ±0.017 | 33 ±6 |
| Logit(Lym)                | 0.063 ±0.018 |           | 0.044 ±0.013 |           |
| Logit(Mon)                | 0.079 ±0.015 |           | 0.086 ±0.020 |           |
| 2. Subtraction index      |          |               |          |               |
| a %Mic−%Nor               | 2.2% ±0.7% | 48 ±11 | 2.6% ±0.7% | 93 ±10 |
| %Mac−%Nor                | 1.1% ±0.3% |           | 0.5% ±0.2% |           |
| b [θMic−θNor]             | 0.015π ±0.004π | 61 ±15 | 0.017π ±0.005π | 99 ±10 |
| [θMac−θNor]               | 0.006π ±0.002π |           | 0.003π ±0.001π |           |
| c** Logit(Neu)−Logit(Lym) | 0.099 ±0.027 | 50 ±18 | 0.109 ±0.029 | 55 ±11 |
| Logit(Mon)−Logit(Lym)     | 0.046 ±0.008 |           | 0.047 ±0.010 |           |

(b) WBC differentials of quality control samples

| WBC differential index | Tests with QC****0810 series (n = 38) | Tests with QC****0811 series (n = 38) |
|------------------------|----------------------------------------|----------------------------------------|
|                        | WBC count: 2921 ± 67/μL | WBC count: 6646 ± 120/μL |
|                        | SD value | SD dispersion | SD value | SD dispersion |
|                        | Mean ±SD  | Mean (%) ±SD (%) | Mean ±SD | Mean (%) ±SD (%) |
| 1. Count ratio index   |          |               |          |               |
| a %Neu                 | 1.2% ±0.1% | 19* ±6 | 1.0% ±0.1% | 24* ±6 |
| %Lym                   | 1.3% ±0.2% |           | 0.8% ±0.1% |           |
| %Mon                   | 0.9% ±0.1% |           | 0.7% ±0.1% |           |
| b Angit(Neu):%Neu      | 0.008π ±0.001π | 11* ±5 | 0.007π ±0.001π | 13* ±6 |
| Angit(Lym):%Lym        | 0.009π ±0.001π |           | 0.006π ±0.001π |           |
| Angit(Mon):%Mon        | 0.009π ±0.001π |           | 0.007π ±0.001π |           |
| c Logit(Neu)           | 0.051 ±0.005 | 38 ±7 | 0.042 ±0.004 | 39 ±9 |
| Logit(Lym)             | 0.056 ±0.007 |           | 0.038 ±0.004 |           |
| Logit(Mon)             | 0.098 ±0.012 |           | 0.074 ±0.011 |           |
| 2. Subtraction index   |          |               |          |               |
| a %Neu−%Lym            | 2.3% ±0.2% | 14 ±8 | 1.6% ±0.2% | 16 ±8 |
| %Mon−%Lym              | 1.9% ±0.3% |           | 1.3% ±0.1% |           |
| b [θMic−θNor]          | 0.015π ±0.001π | 6 ±5 | 0.010π ±0.001π | 6 ±5 |
| [θMac−θNor]            | 0.015π ±0.002π |           | 0.011π ±0.001π |           |
| c** Logit(Neu)−Logit(Lym) | 0.096 ±0.010 | 22 ±8 | 0.067 ±0.007 | 25 ±9 |
| Logit(Mon)−Logit(Lym)  | 0.132 ±0.018 |           | 0.097 ±0.012 |           |

Notes: The measurement uncertainty in flow cytometric RBC and WBC count data was evaluated with 38 courses of two different series of quality control checks by an XE-5000 analyzer. This statistical summary verified that the Angit(p) function standardized measurement uncertainty in the count ratio index most effectively for both RBC size differentials and WBC differentials. Next, the discrepancy in the subtraction index shown in Figure 1 was confirmed statistically and might be derived from the propagation of some type of uncertainty other than precision. We guessed that the instability of accuracy in the count ratio index, which would amplify or offset the uncertainty propagation in the calculated subtraction index, might occur easily in our RBC size differentials method due to fixed gating.

*Statistical significance was verified with Wilcoxon signed-rank test.

**Subtraction of Logit(ratio) equals Log(Odds ratio).
indicate that the increase in the θMeg line from 0.10 to 0.20π required approximately one month in Case 1 but only 10 days in Case 3. Similarly, the durations of the notable microcytic states were 32 days in Case 2 but only 8 days in Case 4. These differences in the change rate with respect to the time scale might be attributable to differences in pathogenesis and the peripheral relative rebalancing between RBC supply (including transfusion) and RBC destruction or loss.

4. Discussion

4.1. Clinical significance of RBC size distribution and their variation with time

With the common application of MCV and RDW in treating anemia, RBC size has been shown to be a useful property for diagnosing pathological erythropoiesis. These indicators are directly affected by the heterogeneity of peripheral RBC populations at any given time because considerable variation has been noted beyond the mean RBC lifespan of approximately 115 days (Cohen et al., 2008; Franco, 2012), which is longer than the lifespans of other blood cells. Therefore, the RBC size distribution is often composed of heterogeneous RBC populations with differing maturation processes and differing ages from enucleation to destruction (Erslev & Beutler, 1995; Quigley et al., 2014). Because partial changes in RBC size distribution can reflect shifts in this balance between RBC supply and RBC age, this approach with trend analyses might improve the understanding of pathogenic
Figure 2. Time-series investigation of erythroid maturation disorders using the XE-5000 analyzer.

Notes: Clinical problem: To identify macrocytic RBC changes associated with erythroid maturation disorders and the recovery phase from marrow suppression using time-series data.

Main relevant results from superimposed RBC size distributions: \[ \text{[fr} = \text{fraction}] \]. Case 1: From Day 1 to 257, Meg-fr increased, whereas Nor-fr decreased; from Day 261 to 330, Nor-fr, Mac-fr and Meg-fr fluctuated widely. Case 2: From Day 52 to 89, conditioning decreased the increased Mac-fr, and Mic-fr (reflecting transfused RBCs) increased to a peak value; from Day 89 to 327, Mac-fr and Nor-fr increased, whereas the peak in Mic-fr diminished. Inferred clinical significance of time-series differential indices: The effects of the DNA synthesis inhibitor (TS-1) medication were more evident in \( \theta \text{Meg} \) than in \( \theta \text{Mac} \) without an overt macrocytic state of \( \theta \text{Mac} - \theta \text{Nor} > -0.02\pi \) in Case 1, whereas RBC immaturity appeared as two separate instances of the macrocytic state before BMT in Case 2. Additionally, there was a transient remarkable peak of the microcytic state of \( \theta \text{Mic} - \theta \text{Nor} > 0\pi \) and subsequent mild elevation in the \( \theta \text{Mac} - \theta \text{Nor} \) index after BMT in Case 2 (areas greater than the cut-off point are shaded.) The turning points of true changes in RBC size distribution related to clinical events such as chemotherapy and blood transfusion were visualized in graphs and were recognized easily. The spike-like changes observed in the \( \theta \text{Mac} - \theta \text{Nor} \) index, as indicated by down arrows in Case 1, might be considered amplified propagation of systematic error because of the presence of synchronized patterns in the RBC size differential graph, which might be induced by the minimal RBC size modification in vitro associated with drip infusion therapies, as shown in Figure 1.
developments affecting background anemic disorders, e.g. various RBC maturation abnormalities or RBC destruction/loss due to hemolysis or bleeding.

4.2. Prerequisite condition for time-series RBC size differential analysis

According to measurement error theory as concerns least-squares fitting (Taylor, 1997), a straight line drawn between two measured values requires the stability of the y-axis precision to be comparable to that of the x-axis of time. Therefore, in considering our variance-stabilizing transformation for standardizing the random error of all measured count ratio values, we emphasized our objective of time-series differences and not improving the measurement precision itself. The adoption of our semi-Angit(p) plot, which was derived to compare time-series cell differential indices based on flow cytometric count data, shares similarities with certain other approaches. For example, in real-time PCR (polymerase chain reaction) measurement procedures, including the serial dilution method, semi-logarithmic graphs are necessary for calibration curves. For our rationale for applying Angit(p) instead of the more widespread Logit(p) function, see Appendices 2 and 3 and the supporting statistical analyses in Table 1. The linear semi-Angit(p) plotting time-series graphs are necessary to attain our objective of linearized statistical analyses in detail, as applied in Figures 2–4.

4.3. Potential isolation of clear clinical trends and hidden systematic error

By indicating substantial relative changes within heterogeneous RBC populations, potentially also quantitatively, time-series RBC size differentials might support the identification of clear pathological trends. Our assumption, based on measurement error theory (Taylor, 1997), suggests that...
time-series trends would output: true pathological change + systematic error + random error. Therefore, if random error propagation can be statistically controlled according to our linearization method, our suggested graphical approach might, in some cases, potentially reveal hidden systematic error through sudden disturbances in otherwise constant trends as typical graphical patterns (see Figure 1). Examples of in vitro systematic error, appearing as a rightward or leftward shift in RBC size distribution, include irregular RBC swelling due to differences in osmotic pressure between plasma with hyperglycemia and the relatively hypotonic counting medium (Strauchen et al., 1981) or cellular membrane abnormalities. Thus, the instability of accuracy in RBC size differentials might occur easily and consequently affect uncertainty propagation in the subtraction index, as shown in Figure 1. It would therefore be necessary to evaluate time-series changes that may include fluctuating systematic error using precision-stabilized semi-Angit(p) plotting graphs.

4.4. Practical approach to evaluate clinical trends in RBC size differentials
We identified early therapeutic responses based on RBC size differentials, which enabled the evaluation of microcytic and macrocytic changes independently. This ability was particularly relevant for anisocytic bimodal distributions, in which the MCV value may be within the normal range (80–100 fl) and RDW might become incalculable, as shown in Case 2 and Cases 5–7. The latent bimodal distributions apparent in these cases suggest that RBC size differentials (1) may help guide the timing or decision for additional treatments; and (2) may enable detailed monitoring of secondary RBC size abnormalities caused by inflammatory and circulatory disorders. As an example of typical use in microcytic anemias, the initial therapeutic response could be monitored based on the decreasing \[\theta_{\text{Mic}} - \theta_{\text{Nor}}\] index as an effect of ferric treatment, whereas an increase in the \[\theta_{\text{Mic}} - \theta_{\text{Nor}}\] index might indicate recurrence of iron deficiency.
4.5. Limitation and future areas of study

Uncertainty propagation in the subtraction index of RBC size differentials will always change erratically according to slight instability in the accuracy of the count ratio index, which might be caused by the fixed gating method of six fractions in RBC size distribution against adjustable gating in WBC differentials. However, quantitative monitoring with subtraction indices, such as the ([MCV−Mac−θ Nor] and [MCV−Mac−θ Mic] indices, might have a significant advantage over objective evaluation of various degrees of anisocytosis from latent levels to overt levels. Therefore, by means of precision-stabilized semi-Angit(p) plotting graphs, we must investigate the clinical trends in each differential index’s lines and simultaneously assess the influence of the instability of accuracy using typical pattern recognition, as above. Additionally, because elevated RDW has recently been investigated as a predictor of mortality in various non-hematological disorders (Cauthen et al., 2012; Hu et al., 2013; Lippi & Plebani, 2014; Montagnana et al., 2012), the RBC size differential method might offer greater RDW-related detail over the clinical courses of cases with poor prognoses. In our view, such cases might be associated with pathological rebalancing between RBC supply and RBC lifespan. Therefore, we hope to investigate these possibilities further via real-time integration of the size differential-time course analysis program into our routine practice to evaluate the initial hematological responsivity under various therapies (Price et al., 2011).

5. Conclusion

This study demonstrates that a clinical monitoring method using time-series RBC size differentials, with measurement precision standardized for reliable difference comparisons, can offer the following advantages: a more detailed RBC size distribution examination complementing the MCV and RDW indicators; an easily visualized, improved representation of anemic disorder treatment; and the possibility of indicating time-series rebalances in daily RBC supply vs. mean RBC age for each size fraction.

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Competing Interests

The authors declare no competing interest.

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Appendix 1

Procedures for data acquisition of RBC size distributions from PNG-format digital images

The probability distributions of each RBC size fraction were obtained by converting the PNG-format digital images output from the analyzer. After subdividing the x-axis into 256 points for compilation in a relational database, the y-value (frequency) of each corresponding x-value (fL) was determined by subtracting the reference height (shown in Figure A1 with red arrow) from the height to the bottom pixel of the volume distribution curve (shown in Figure A1 with green arrow). Figure A1. How RBC size distributions are obtained from digital image data (Appendix 1). Our method obtained data digitally using the XE-5000 analyzer’s output PNG-formatted images. Figure A1 shows the x-axis composition of 256 pixels and how the y-value of each x-value is determined by 1) locating the pixel at the bottom of the volume distribution graph’s light blue line (green arrow); and 2) finding the height difference between the green arrow and the reference red arrow.

Next, the zero-point for all RBC volume histograms was determined statistically by comparing the mean value calculated from all histograms with the corresponding mean value from all analyses reported for MCV by one-channel increments. This resulted in an origin shift to the right by 1 fL. All probability distribution-related calculations, from 41 to 160 fL, were performed again after zero-point adjustment and were once again compiled in a relational database such that each channel value was equivalent to the corresponding original femtoliter value.

Appendix 2

Induction of error variance stabilizing transformation for estimating the count ratio measurement uncertainties

The cytometric blood cell count method is considered random sampling without replacement, such that the cell count number x follows a hypergeometric distribution. Furthermore, if the measured total count number n is sufficiently large and constant, as is certainly the case, such a hypergeometric distribution can be approximated by the simpler binomial distribution.

Thus, for the variance of cell count ratio p, the division of x by n can be expressed as follows:
If the true value and the uncertainty of the measured value of count ratio \( p \) are represented as \( \hat{p} \) and \( \delta p \), respectively:

\[
\frac{p(1-p)}{n}
\]

Next, according to the “Delta method” (Oehlert, 1992), taking the variance of both sides yields the following:

\[
V[p] = V[\hat{p} + \delta p] = V[\hat{p}] + V[\delta p] = V[\delta p] = \frac{p(1-p)}{n}
\]

Next, the error variance stabilizing function \( f(p) \), which estimates

\[
V[f(p)] = \text{Const, is given by the following:
}

\[
f'(p) = \sqrt{\frac{\text{Const} \cdot n}{p(1-p)}} \approx f'(p)
\]

\[
f(p) = \sqrt{\text{Const} \cdot n \cdot \frac{p}{\sqrt{u(1-u)}}} = 2 \sqrt{\text{Const} \cdot n \cdot \arcsin \sqrt{p}}
\]

Thus, given that the total count number \( n \) is constant, we can conclude the following:
\[ f(p) = 2 \cdot \arcsin \sqrt{p} \]

In contrast to the Logit function used in logistic analysis, we call this function Angit(p), with the transformed value defined as the angle ratio \( \theta \), as below:

\[ \theta = \text{Angit}(p) = 2 \cdot \arcsin \sqrt{p}, \]

where the value of the angle ratio \( \theta \) varies from 0 to \( \pi \) such that we define the unit of angle ratio \( \theta \) as \( \pi \) and set the range of variable \( \theta \) as simply 0 to 1.

**Appendix 3**

The propagation of uncertainty in angular transformation vs. Logit transformation

The variance of the count ratio \( p \), expressed as \( V(dp) \), is equal to \( \frac{p(1-p)}{n} \)

because the cytometric RBC count ratio \( p \) can be approximated as a binomial distribution, where the total count number \( n \) is constant.

Based on the relationship \( d\text{Angit}(p) = \frac{dp}{\sqrt{p(1-p)}} \) and substituting \( \frac{p(1-p)}{n} \) for \( V(dp) \),

the error variance of \( \text{Angit}(p) \) with angle ratio \( \theta \) is estimated as below:

\[
V[\text{Angit}(p)] = V[d\text{Angit}(p)] = V\left[ \frac{dp}{\sqrt{p(1-p)}} \right] = \frac{1}{p(1-p)} \cdot V[dp] = \frac{1}{p(1-p)} \cdot \frac{p(1-p)}{n} = \frac{1}{n}
\]

**Conclusion:** The error variance of \( \text{Angit}(p) \) is not affected by the quantity of the count ratio \( p \) and thus is constant.

The error variance of \( \text{Logit}(p) \) is estimated as below, with the same \( V(dp) \) substitution as above:

\[
V[\text{Logit}(p)] = V[d\text{Logit}(p)] = V\left[ \frac{dp}{p(1-p)} \right] = \left( \frac{1}{p(1-p)} \right)^2 \cdot V[dp] = \left( \frac{1}{p(1-p)} \right)^2 \cdot \frac{p(1-p)}{n} = \frac{1}{np(1-p)}
\]
Conclusion: The error variance of Logit(p) can be near-stable in a p range such as [0.2, 0.8]; however, it is clear from the denominator alone that the instability is very high as p approaches 0 or 1.

As transformations of the same input variable, the Angit(p) and Logit(p) functions can be visualized and compared geometrically as well (see Figure A2). In the evaluation of cell count data by flow cytometry, it would be important to apply these transformations properly; Angit(p) appears applicable to the entire range of p for a precision-stabilized scale that is linear, whereas Logit(p) appears to be a useful linear-like operator only within an approximate p range of 0.2–0.8. Figure A2. Geometric relationships between the Angit transformation and Logit transformation shown in a semicircular model.

The diagram above shows the geometric relationships among count ratio p, Angit(p) and Logit(p) based on the assumption of Bernoulli trials with the variance $\sigma^2 = p(1-p)$. 1. Angit(p) = twice the length of arc OR(Arc) = $\theta$. 2. Logit(p) = twice the natural log of line segment OS(p/$\sigma$). Thus, Angit(p) indicates the standardization of the difference in probability p using Arc; by contrast, Logit(p) indicates the standardization of the relative ratio in likelihood p/$\sigma$ using the natural log of p/$\sigma$. 