INFORMATION CONSUMPTION BY
REISSNER-NORDSTROM BLACK HOLES

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ABSTRACT: The low-energy scattering of charged fermions by extremal magnetic Reissner-Nordstrom black holes is analyzed in the large-$N$ and $S$-wave approximations. It is shown that (in these approximations) information is carried into a causally inaccessible region of spacetime, and thereby effectively lost. It is also shown that there is an infinite degeneracy of quantum black hole ground states, or “remnants”, which store — but will not reveal — the information. A notable feature of the analysis — not shared by recent analyses of dilatonic black holes — is that the key physical questions can be answered within the weak coupling domain. We regard these results as strong evidence that effective information loss occurs in our universe.
INTRODUCTION

Extremal black holes provide a simple laboratory in which to study quantum mechanical aspects of black holes. There are three general possibilities which have been discussed for the outcome of a scattering experiment in which a particle is sent into an extremal black hole and Hawking re-emitted:

I) The scattering is unitary, with a finite number of quantum states for the black hole.

II) The scattering is unitary with an infinite number of asymptotic quantum states of the black hole, or “remnants”.

III) The scattering is not unitary, and information is destroyed.

Extensive analyses of extremal black holes in dilaton gravity at large $N$ over the last year [CGHS] show no evidence that possibility (I) might be realized, while recent work [bos] has shown that possibility (II) and (III) are much less distinct than previously suspected.

One feature of the large-$N$ analysis of dilatonic black holes has been in some ways disappointing: Gravitational collapse inevitably leads to a singularity at which the large-$N$ approximation breaks down. Fortunately some key physical questions are not affected by this breakdown. For example possibility (I) can still be ruled out at large $N$. However, one can not determine which of possibilities (II) or (III) are realized without solving a strongly coupled quantum problem.

We were thus motivated to search for a model in which possibility (II) is demonstrably realized at weak coupling†. After running around in several circles we realized that such a model was under our noses: real-world magnetic Reissner-Nordstrom black holes. Although the structure of their extremal ground state is much more complex than that of their dilatonic cousins, they have two big advantages: large-$N$ can tame their dynamics, and they exist as solutions to the Einstein-Maxwell equations, without the introduction of unobserved fields such as a dilaton.

We wish to study long-wavelength scattering of $S$-wave charged fermions by an extremal Reissner-Nordstrom black hole with a large magnetic charge and radius, both given by $Q$ (we take $Q > 0$). To render this problem tractable, we make the $S$-wave approximation in which all higher angular modes are suppressed. Naively one expects that, at wavelengths large relative to $Q$, this approximation is good. However, unlike the dilatonic case studied in [CGHS], there are several subtleties which have so far prevented a

† See [bol] for related efforts.
careful justification of the approximation, and we cannot be sure that it is valid†. For
$N + 1$ flavors of fermions the effective two-dimensional $S$-wave theory is described by

$$S = \frac{1}{2\pi} \int d^2 \sigma \sqrt{-g} \left[ e^{-2\phi} R + 2 e^{-2\phi} (\nabla \phi)^2 + 2 - 2Q^2 e^{2\phi} - \frac{1}{2} \sum_{i=1}^{N} (\nabla f_i)^2 \right]. \quad (actn)$$

The two-dimensional metric appearing in (actn) is related to the four dimensional metric
by $ds^2 = g_{\alpha\beta} d\sigma^\alpha d\sigma^\beta + e^{-2\phi} d^2 \Omega$, with $\alpha, \beta$ ranging over $(r, t)$. The scalar field $\phi$ measures
the (logarithm of) the area of two spheres of constant radius. The first four terms in
(actn) arise directly from dimensional reduction of the four-dimensional Einstein-Maxwell
action. The last term arises from the bosonization of fermion $S$-wave modes studied by
Callan and Rubakov [crv] in GUT theories. One charged linear combination of the original
$N + 1$ flavors acquires a mass from electromagnetic effects. The dynamics of this mode was
studied for dilaton black holes in [alf], but because of its mass it decouples at sufficiently
low energies. The two-dimensional relic of the four-dimensional gauge field is suppressed in
(actn), as it cannot be excited by the neutral fields and so may be consistently neglected.
Previous work on the model defined in (actn) and related models obtained by dimensional
reduction can be found in [prev] and [trv].

One might hope that for large $Q$ particle-hole scattering could be adequately analyzed
in a semiclassical loop expansion of the reduced theory, but in fact large $N$ will be needed
in addition to the $S$-wave approximation, for several reasons. First, as pointed out in
[PSSTW], the temperature fluctuations of a near-extremal charged black hole go as

$$\Delta T \sim \left[ \frac{\hbar}{\sqrt{M - Q}} \right]^2, \quad (tfl)$$

so the leading semiclassical formula for the temperature (and radiation rate) becomes
unreliable very near extremality. But in the large-$N$ limit, where $\hbar \to 0$ (while $N \to \infty$

† One subtlety is that incoming long-wavelength modes may produce regions of high curva-
ture either near the origin or the inner Cauchy horizon. We shall argue later that these
regions are irrelevant to the issue of effective information loss. Another subtlety has to
do with the fact that the centrifugal barrier seen by the higher partial waves turns off
near the horizon. This means firstly that there are an infinite number of short-distance
but low-energy modes near the horizon. We believe these should not be present in a long-
distance effective theory, but we do not know how to define such a theory in a manner
consistent with Lorentz invariance and energy conservation. It also means that there are
long-distance low-energy higher angular momentum modes near the horizon which might
be excited as quantum fluctuations. As was discussed in [trv] the tidal forces seen by these
modes - unlike the s-wave - blow up at the horizon, thus once excited they might have
consequences which are unaccounted for in the s-wave approximation.
keeping $Nh$ fixed) we see that

$$\frac{\Delta T}{T} \to 0,$$

so that near-extremal black holes are indeed characterized by a definite temperature.

A second problem with the loop expansion was discussed in [trv]. For a non-extremal Reissner-Nordstrom black hole, the one-loop contribution to the expectation value of the stress tensor diverges on the inner (but not the outer) horizon. This is related to the classical instability of the inner horizon, as studied in many papers [hrz]. This divergence persists, albeit in a softened form, in the extremal limit in which the two horizons coalesce. Since the one-loop corrections are divergent, the loop expansion is clearly unreliable.

Although frightening at first, these divergences are in fact rather benign and can be controlled within the $1/N$ expansion. The leading large-$N$ equations, in which one-loop quantum back reaction is included, have solutions which are in a sense “near” to corresponding classical solutions. In particular [trv], there is an extremal, zero-temperature ground-state solution with causal structure identical to that of the classical solution. The large-$N$ geometry is near to its classical counterpart, but third and higher derivatives of the fields are divergent near the horizon. We shall see in this paper that divergences encountered in particle-hole scattering are also benign, although the behavior of the stress tensor near the horizon leads to an unexpected non-analytic large-$N$ mass-area relationship, which differs from the classical result even at large $Q$ sufficiently near extremality.

**CALCULATION**

Previous analyses of large-$N$ two dimensional gravity have been largely carried out in conformal gauge. This gauge is somewhat awkward in the present context. For example even the classical solutions are known only implicitly in this gauge. A more convenient choice is light-cone gauge†, for which the two dimensional metric takes the form

$$ds^2 = -h(dv)^2 + 2drdv,$$  \hspace{1cm} (lcm)

$\sqrt{-g} = 1$ and the scalar curvature is $R = -\partial^2_r h$. In this gauge one can solve the classical equations and obtain an analytic expression — known as the Vaidya metric — for arbitrary null infalling matter, characterized by a stress tensor obeying $T_{ra} = 0$:

$$h = 1 - \frac{2M(v)}{r} + \frac{Q^2}{r^2},$$  \hspace{1cm} (rdya)

† Previous light-cone gauge analyses of dilatonic black holes can be found in [leg].
where $2 \partial_v M = T_{v v}$. The large-$N$ trace and dilaton equations may then be written in the form

$$
\Box \phi = \partial_r \Sigma = \Sigma \partial_r U + \frac{Q^2 e^{4 \phi} (1 + \gamma e^{2 \phi})}{(1 - \gamma e^{2 \phi})} - \frac{e^{2 \phi}}{1 - \gamma e^{2 \phi}}, \quad \text{(pheeq)}
$$

$$
R = -\partial_r^2 h = \frac{2}{1 - \gamma e^{2 \phi}} \left[ e^{2 \phi} - 2 Q^2 e^{4 \phi} - \Sigma \partial_r \phi \right], \quad \text{(heq)}
$$

where

$$
\Sigma \equiv 2 \partial_v \phi + h \partial_r \phi,
$$

$$
U \equiv 2 \phi - \frac{1}{2} \ln(1 - \gamma e^{2 \phi}), \quad \text{(ueq)}
$$

and

$$
\gamma = \frac{Nh}{24}. \quad \text{(gamma)}
$$

A future (past) apparent horizon is a zero of $\Sigma$ ($\partial_r \phi$), which implies $(\nabla \phi)^2 = 0$. One important linear combination of the constraint equations is local

$$
e^{2 \phi} l^a l^b T^Q_{ab} \equiv \frac{1}{2} \gamma e^{2 \phi} \left( \frac{1}{2} h \partial_r^2 h - \frac{1}{4} (\partial_r h)^2 + \partial_v \partial_r h \right)
= \partial_v \Sigma + \frac{h}{2} \partial_r \Sigma - \frac{1}{2} \Sigma^2 - \frac{1}{2} \partial_r h \Sigma, \quad \text{(vv)}
$$

where the components of the null vector $l$ are $(l^r, l^v) = (h/2, 1)$. Fortunately, the other linear combination, which is non-local, shall not be needed.

The extremal solutions were studied in [trv] and found to be of two kinds referred to therein as the even and odd extensions. Here we shall focus on the odd extension, which reduces to the classical solution as $h \to 0$, and denote it as $\phi_0(r)$ and $h_0(r)$ †. This solution has a timelike singularity at the “origin” where $e^{-2 \phi_0} = \gamma$. Near the horizon $r_H$, it was shown [trv] that the fields have the non-analytic behavior

$$
\phi_0 - \phi_H = \beta x |x|^{\delta},
$$

$$
h_0 = \alpha_1 x^2 + \alpha_2 x^3 |x|^{\delta}. \quad \text{(teexp)}
$$

Where $\phi_H \equiv \phi(r_H)$, $x \equiv r - r_H$ and

$$
\delta = \frac{3}{2} \left[ \sqrt{1 + \frac{8 \gamma}{3 (e^{-2 \phi_H} - \gamma)}} - 1 \right], \quad \text{(deltriv)}
$$

with

$$
e^{-2 \phi_H} = Q^2 \left[ \frac{1 + \sqrt{1 + \frac{4 \gamma}{Q^2}}}{2} \right]. \quad \text{(phih)}
$$

† The even solutions are in many ways more interesting since they correspond to spacetimes free from any malevolent singularities. But their stability and response to perturbations cannot be studied in the approximations used here.
δ tends to zero for large Q. To leading order in $\frac{\gamma}{Q^2}$

\begin{align*}
\alpha_1 &= \frac{1}{Q^2}, \\
\alpha_2 &= -\frac{2}{Q^3}, \\
\beta &= -\frac{1}{Q}, \\
r_H &= Q,
\end{align*}

and

\begin{equation}
e^{-\phi_H} = Q.
\end{equation}

While for large Q one can safely use these approximations to $\alpha_1$, $\alpha_2$, $\beta$, $r_H$ and $\phi_H$, we do not omit terms subleading in $1/Q$ in the expression for $\delta$ because such an approximation would break down very near the horizon (at $x$ less than of order $Q e^{\exp(-Q^2/\gamma)})$. The non-analyticity in (texp) leads to divergences for example in the second derivative of the curvature.

Let us now consider an incoming matter shock wave† along $v_0$ whose classical stress tensor obeys

\begin{equation}
l^{a}l^{b}T_{ab}^f = 2\mu\delta(v-v_0).
\end{equation}

We wish to compute, following [BDDO], $\phi$ and $h$ perturbatively in $\mu$ in a Taylor expansion above the shock wave. $\phi$ is continuous across the shock wave, while $h$ has a discontinuity which is determined by the constraints and is classically equal to $-\frac{2\mu}{r}$. $\Sigma$ (defined in (ueq)) also has a discontinuity $\delta\Sigma$ across $v_0$, which, according to (phec), obeys

\begin{equation}
\partial_r(e^{-U}\delta\Sigma) = 0.
\end{equation}

The integration constant is determined from the asymptotic boundary condition $\delta\Sigma \to \frac{2\mu}{r^2}$. One thereby obtains

\begin{equation}
\delta\Sigma = 2\mu e^U.
\end{equation}

Near the horizon $r_H$, $\Sigma_0$ (the value of $\Sigma$ below the shock wave) has a higher order zero:

\begin{equation}
\Sigma_0 \approx \alpha_1\beta(1+\delta)x^2|x|^{\delta}.
\end{equation}

† Note that there is an issue of orders of limits here: we take $N \to \infty$ before $\mu \to 0$.

† Strictly speaking shock waves are not allowed in the long-distance effective field theory, but the case of a smooth pulse is qualitatively similar.
Since $\delta \Sigma$ is non-zero at $r_H$, this zero is split into two simple zeros which are (by definition) the inner and outer apparent horizons, as illustrated in the figure. To leading order in $\frac{Q}{\mathcal{Q}^2}$ and $\frac{\mu}{Q}$ one finds that the locations of the horizons are given by

$$r_\pm \approx r_H \pm Q \left( \frac{2\mu}{Q} \right)^{\frac{1}{1+\delta}}.$$  \hspace{1cm} (rpm)

Comparing with (texp) and recalling that the dilaton measures the area of the two spheres, we see that the area $A_H$ of the outer horizon obeys

$$A_H - A_0 \simeq 8\pi Q^2 \left( \frac{2\mu}{Q} \right)^{\frac{1+\delta}{1+\delta}},$$  \hspace{1cm} (mar)

where $A_0$ is the extremal area. Thus the mass-area relation is non-analytic. Notice that no matter how small $\delta$ is, there is always some value of $\mu \ (\mu \sim Qe^{-\frac{1}{3}})$ below which (mar) is not well approximated by the classical relation $A_H - A_0 \sim 8\pi \sqrt{2\mu Q^3}$.

The mass of the black hole will of course decrease due to Hawking radiation and we expect it to settle back to extremality. To study this, we first calculate the trajectories of the two apparent horizons, denoted by $\hat{r}_\pm$. We again work to leading order in $\frac{Q}{\mathcal{Q}^2}$ and $\frac{\mu}{Q}$.

Since $\Sigma$ vanishes along $\hat{r}_\pm$ one has

$$\partial_v \Sigma = -\partial_r \Sigma \partial_v \hat{r}_\pm.$$ \hspace{1cm} (slope)

Now (mgu) and (hoz) imply that

$$\partial_r \Sigma(r_\pm) \simeq \pm \frac{2}{Q^2} \left( \frac{2\mu}{Q} \right)^{\frac{1+\delta}{1+\delta}}.$$ \hspace{1cm} (dersx)

Similarly (vv) implies that at $r_\pm$

$$\frac{h}{2} \partial_r \Sigma + \partial_v \Sigma = \gamma e^{2\phi} \left( \frac{h_0}{2} \partial_r^2 \delta h + \frac{\delta h}{2} \partial_r^2 h_0 - \frac{1}{2} \partial_r h_0 \partial_r \delta h + \partial_v \partial_r \delta h \right) + e^{2\phi} \mu Q \partial_r Q.$$ \hspace{1cm} (vvtwo)

It turns out that the dominant contribution for small $\mu$ is given by the second term on the right hand side, which involves $\delta h$ with no derivatives. To evaluate this term we need to know $\delta h$ just above the shock wave which, according to (heq) obeys

$$\partial_r^2 \delta h = \frac{2\partial_r \phi \delta \Sigma}{1 - \gamma e^{2\phi}},$$ \hspace{1cm} (rrh)

so that

$$\delta h = 4\mu \int dr \frac{1}{\gamma} \left( -1 + \frac{1}{\sqrt{1 - \gamma e^{2\phi}}} \right).$$ \hspace{1cm} (dhm)
(The integration constants are fixed by the requirement that $\delta h$ asymptotically vanish.) Furthermore, to leading order $h \partial_r \Sigma$ vanishes so that (vvtwo) reduces to

$$\partial_v \Sigma(r_\pm) \simeq -\frac{\gamma \mu}{Q^5}. \quad (sigv)$$

(slope) and (rpm) then imply that right above the shock wave

$$\partial_v \hat{r}_\pm \simeq -\frac{\gamma (\hat{r}_\pm - r_H)}{4Q^2}. \quad (sltwo)$$

To proceed further, we evoke the adiabatic approximation in which the black hole is taken to evolve slowly so that its dynamic geometry may be approximated by a sequence of static ones. We expect the adiabatic approximation to be good for large $Q^2$, but have been unable to carefully justify this. In this approximation (sltwo) continues to hold everywhere along $\hat{r}_\pm$. Thus the inner horizon moves out towards $r_H$ while the outer horizon moves in towards $r_H$, and the black hole exponentially approaches its extremal ground state. Note however that while the black hole is excited, the trajectories of $\phi = \phi_H$ and $r = r_H$ are spacelike. The event horizon therefore is shifted outward (relative to the original apparent horizon) by the scattering process, as illustrated in the figure.

Also, within the adiabatic approximation (rpm) relates the position of the outer horizon $r_+$ to $\mu$. (sltwo) then implies that

$$\partial_v \mu \simeq -\frac{\gamma}{2Q^3} \mu, \quad (rmls)$$

so that the mass decays exponentially back to its extremal value as

$$\mu(v) \simeq \mu e^{-\frac{\gamma(v-v_0)}{2Q^3}}. \quad (mxp)$$

There are two regions in which the large $N$ equations used here cannot be trusted. The first is near the origin $e^{2\phi} = \gamma$, where the curvature becomes large and higher-dimension corrections to the Einstein-Maxwell theory are important. The second is the future Cauchy horizon, or the extension of $I^+$ inside the event horizon. An observer inside the black hole crosses this Cauchy horizon in finite time, yet is able to see all of the universe outside the black hole before doing so. There is therefore a large energy concentration near this surface, the effects of which are subtle and have been analyzed in many papers [hrz].

Fortunately, physics outside the horizon is insensitive to the (intractable) behavior of the system in these regions. To see this, consider a Hamiltonian $H$ which evolves along
the series of spacelike slices asymptotic to the slice $\Sigma = \Sigma_I \cup \mathcal{I}^+$ where, as depicted in the figure, $\Sigma_I$ is a spacelike surface inside the horizon. These slices can be chosen to completely cover the spacetime outside the horizon. $\Sigma_I$ can be chosen so that it avoids the difficult region near the future Cauchy horizon, and so that the intersection of the shock wave with $\Sigma_I$ is in weak coupling. Although $\Sigma_I$ extends into the strong coupling region near $e^{2\phi} = \gamma$, this does not present any difficulties because the system is unexcited in that region. The non-trivial dynamics are everywhere weakly coupled for all time, and our approximations should be valid.

**DISCUSSION**

We now argue that our results imply that an arbitrarily large amount of information can be sent into the black hole, and will never emerge again in the universe from which it was thrown in. The black hole relaxes to extremality with a characteristic time

$$t_c = \frac{Q^3}{\gamma}.$$  

Consider experiments in which an arbitrarily large number of wavepackets are sent in from $\mathcal{I}^-$ spaced at intervals of $t_c$ seconds. In the process, an arbitrarily large amount of information is sent in. In order for no information loss to occur, in the asymptotic future, all correlations between the state inside and the state outside the horizon should be destroyed. This can occur only if the state inside is unique and independent of the initial state of the infalling matter. The preceding analysis shows that nothing catastrophic happens to the infalling matter as it crosses the apparent horizon so in the asymptotic future the state inside the event horizon (on $\Sigma_I$) will depend heavily on the incoming scattering state. Indeed, since the system is still weakly coupled on $\Sigma_I$, the quantum state of the left-moving conformal $f$-matter will be essentially the same as on $\mathcal{I}^-$. Thus in the course of this experiment an arbitrarily large amount of information will be carried into the causally inaccessible region inside the event horizon and thereby be effectively lost.

It is also evident that, with respect to the time slicing described above, this is a theory with an infinite number of remnants. What we mean by this statement is that there are an infinite number of solutions of the large-$N$ constraint equations on a spacelike slice which are identical outside the horizon, but have differing $f$-matter configurations inside the horizon, corresponding to an infinite degeneracy of large-$N$ semiclassical quantum states.\footnote{Actually, if we enforce the constraint that the incoming matter excitations are long wavelength on $\mathcal{I}^-$ - in accord with our approximations - this would not be the case because the...}
However it is important to note that the interpretation that the information is stored in these remnants may be dependent on the slicing. For example we might have chosen the asymptotic interior surface $\Sigma_I$ so that the $f$-wave arrives at the singularity before intersecting $\Sigma_I$. In this case it is a logical possibility that the information is destroyed when it arrives at the singularity, in which case one would not conclude that the information is stored inside the black hole†.

Of course, physics outside the event horizon cannot, by causality, depend on the choice of slicing inside the event horizon, which we are therefore free to choose for our own convenience. Consequently the observer outside the horizon cannot possibly distinguish between actual information loss and storage by remnants. The choice of slicing made in this paper was motivated by the desire to avoid the difficult dynamics near the singularity, and it is consistent with this choice to describe the theory as having an infinite number of remnants.

We should note that although the calculations above were carried out in the $N \to \infty$ limit all the important conclusions continue to hold when $N$ (or $Q$) is sufficiently large but finite. The distinction is important to make because when $N \to \infty$, $\hbar \to 0$, so that the Bekenstein-Hawking entropy of the black hole - which goes as $\frac{1}{\hbar}$ - goes to $\infty$. Thus it might be claimed that our conclusions are simply a consequence of working in a limit where the ground state is infinitely degenerate and that at finite $N$ there would be an upper limit on the information the black hole can carry and a finite number of remnants. Finite $N$ differs from $N \to \infty$ in that we have to keep track of the quantum fluctuations in the metric and dilaton, and these might be potentially large close to the horizon. But the larger $N$ is, the closer one must approach the horizon in order for these effects to be significant.

incoming matter excitations must be late enough so that they are still in weak coupling when they arrive at $\Sigma$, yet early enough to avoid a potential pile up of energy density near the future Cauchy horizon. There are only a finite number of states in this finite interval above any given wavelength. This problem can be avoided by choosing a different surface $\Sigma_H$ defined as the (spacelike or null) surface along which $\phi$ takes the constant value $\phi_H$ characterizing the horizon of an unperturbed extremal solution. This is a geodesically complete surface which is everywhere in weak coupling. Since any finite point on $\Sigma_H$ is an infinite distance from $i^+$, there is clearly no pile up of energy density. Furthermore, because the event horizon is moved out by each scattering process, this surface is well behind the event horizon if many $f$-particles (and much information) are thrown in to the black hole. The potentially infinite amount of information on $\Sigma_H$ is therefore unavailable to an observer on $I^+$.

† Another possibility is that boundary conditions might be specified at the timelike singularity to reflect the matter - and the information - up to the future Cauchy horizon and possibly on to the next universe. In this case all the information will be present on $\Sigma_I$ no matter how it is chosen.
Similarly, the adiabatic approximation would break down for finite $N$ sufficiently close to extremality. But again for large enough $N$ this occurs only very near extremality. Thus by sending in energy at a judicious rate, for $N$ large but finite, one could keep the black hole close enough to extremality ($\frac{\mu}{Q}$ small enough) for our approximations to hold, but far enough from extremality for the finite $N$ effects to be insignificant at the apparent horizons. The black hole would then respond according to the calculations above except for the first moments after it departs from extremality and the last moments before finally settling down. We would thus conclude that even for finite $N$ (when the entropy is finite) that the black hole can consume an arbitrarily large amount of information and store it in an infinite number of remnant states.

Finally, one may be concerned that this infinite degeneracy of states will lead to divergent black hole pair production rates. In fact magnetic black hole pair production was computed semiclassically in [gast] and found to be finite. The reason for this was discussed at length in [bos]: extremal black holes do not behave quantum mechanically like elementary particles.

Thus we have found a system which can be seen — without resorting to speculations about strong coupling dynamics — to solve the information puzzle by storing it in an infinite degeneracy of black hole quantum states. Further this two-dimensional system might be a good approximation to real-world long-wavelength fermion-magnetic black hole scattering.

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REFERENCES

hrz. J.M. McNamara, Proc. R. Soc. London A358, 449 (1978); A364, 121 (1978); Y. Gürsel, V.D. Sandberg, I.D. Novikov, and A.A. Starobinsky, Phys. Rev. D19, 413 (1979); R.A. Matzner, N. Zamorano, and V.D. Sandberg, ibid. 19, 2821 (1979); S. Chandresekhar and J.B. Hartle, Proc. R. Soc. London A284, 301 (1982); N.
Zamorano, Phys. Rev. D26, 2564 (1982); E. Poisson and W. Israel, Phys. Rev. Lett. 63, 1663 (1989); Phys. Lett. B233, 74 (1989); Phys. Rev. D41, 1796 (1990); A. Ori, Phys. Rev. Lett. 67, 789 (1992).

gast. D. Garfinkle and A. Strominger “Semiclassical Wheeler Wormhole Production” Phys. Lett. B256, 146 (1991).

leg. H. Terao “Two-Dimensional Black Hole Evaporation in Light-Cone Gauge” Kanazawa preprint 92-19 (1992). X. Shen “Quantum Dilaton gravity in Light-Cone Gauge” Cern preprint TH-6633 (1992).

CGHS. C.G. Callan, S.B. Giddings, J.A. Harvey and A. Strominger, “Evanescent Black Holes”, Phys. Rev. D45, R1005 (1992); For recent reviews see J.A. Harvey and A. Strominger, “Quantum Aspects of Black holes” preprint EFI-92-41, hep-th@xxx/9209055, to appear in the proceedings of the 1992 TASI Summer School in Boulder, Colorado, and S.B. Giddings, “Toy Models for Black Hole Evaporation” preprint UCSBTH-92-36, hep-th@xxx/9209113, to appear in the proceedings of the International Workshop of Theoretical Physics, 6th Session, June 1992, Erice, Italy.

BDDO. T. Banks, A. Dabholkar, M.R. Douglas and M. O’Loughlin, “Are Horred Particles the Climax of Hawking Evaporation?”, Phys. Rev. D45, 367 (1992); J.G. Russo, L. Susskind and L. Tholacius, “Black Hole Evaporation in 1 + 1 Dimensions”, Phys. Lett. B292, 13 (1992).

PSSTW. J. Preskill, P. Schwarz, A. Shapere, S. Trivedi and F. Wilczek, Mod. Phys. Lett. A6, 2353 (1991).

bol. T. Banks and M. O’Loughlin “Nonsingular Lagrangians for Two Dimensional Black Holes” Rutgers preprint RU-92-61 (1992).

bos. T. Banks, M. O’Loughlin and A. Strominger “Black Hole Remnants and the Information Puzzle” hep-th/9211030, Phys. Rev. D to appear.

prev. M. McGuigan, C. R. Nappi and S. A. Yost, “Charged Black Holes In Two Dimensional String Theory” IASSNS-HEP-91/57; O. Lechtenfeld and C. R. Nappi, “Dilaton Gravity and No Hair Theorem in Two Dimensions” IASSNA-HEP-92-22; D.A. Lowe, “Semiclassical Approach to Black Hole Evaporation” PUPT-1340.

trv. S. Trivedi “Semiclassical Extremal Black Holes” Caltech preprint CALT-68-1833 (1992).

alf. M. Alford and A. Strominger ”S-Wave Scattering of Charged Fermions by a Magnetic Black Hole” Phys. Rev. Lett 69, 563, 1992.
Crv. C. Callan, Phys. Rev. D25 (1982) 2141; Phys. Rev. D26 (1982) 2058; Nucl. Phys. B212 (1983) 391; V. Rubakov, Pis’ma Zh. Eksp. Teor. Fiz. 33 (1981) 658 (JETP Lett. 33 (1981) 644); Nucl. Phys. B203 (1982) 311.

ted. T. Jacobson “Black Hole Evaporation and Ultrashort Distances” Phys. Rev. D 44 (1991) 173; “Black Hole Radiation in the Presence of a Short-Distance Cutoff” UMDGR93-32, ITP preprint (1993).

FIGURE CAPTION

Figure 1. A shock wave incident on an extremal Reissner-Nordstrom black hole splits the apparent horizon $r_H$ into a pair of apparent horizons $r_{\pm}$, which then exponentially decays back to $r_H$. The even horizon is outside $r_H$. The asymptotic spacelike surface $\Sigma$ is positioned so that the shock wave intersects it at large radius and weak coupling, and it avoids the Cauchy horizon.