125 GeV Technidilaton at the LHC

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The technidilaton (TD) is a composite scalar predicted in walking technicolor (WTC), arising as a pseudo Nambu-Goldstone boson associated with the spontaneous breaking of the approximate scale invariance. Due to the Nambu-Goldstone boson’s nature, the TD can be as light as the LHC boson that has been discovered at around 125 GeV. We discuss the size of the TD mass and the coupling properties relevant to the LHC study. It turns out that the TD couplings to the standard model (SM) particles take the same form as those of the SM Higgs boson, except the essentially distinguishable two ingredients: i) the overall coupling strengths set by the decay constant related to the spontaneous breaking of the scale invariance, which is in general not equal to the electroweak scale; ii) the couplings to photons and gluons which can include extra contributions from technifermion loops and hence can be enhanced compared to the SM Higgs case. To be concrete, we take the one-family technicolor model to explore the TD LHC phenomenology at 125 GeV. It is shown that the TD gives the signal consistent with the currently reported LHC data, notably can explain the excess in the diphoton channel, due to the extra contributions to digluon and diphoton couplings coming from the one-family technifermion loops.

1. Introduction

On July 4, 2012, a new particle at around 125 GeV was discovered at the LHC.1 Through measurements of the coupling property, spin and parity, the new particle has so far been almost consistent with the Higgs boson predicted as a key boson responsible for the origin of mass in the standard model (SM). One discrepancy from the SM Higgs has been, however, reported in the diphoton channel2 where the observed signal event is about two times larger than the SM Higgs prediction. This would imply that the observed scalar boson is a SM-Higgs impostor concerning the underlying theory beyond the SM.

One such a possible impostor is the technidilaton (TD), a composite scalar boson, predicted in the walking technicolor (WTC)3,4 with an approximately scale-invariant (conformal) gauge dynamics and a large anomalous dimension $\gamma_m = 1$. The TD is a pseudo Nambu-Goldstone boson for the spontaneous breaking of the approximate scale symmetry triggered by technifermion condensation and hence its lightness, say 125 GeV, would be protected by the approximate scale symmetry

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inherent to the WTC. Thus the discovery of TD would imply the discovery of the WTC.

The LHC signatures of the TD were studied in a couple of recent papers.\textsuperscript{5–7} It was shown\textsuperscript{6} that the 125 GeV TD is consistent with the currently reported diphoton signal as well as other signals such as $WW^*$ and $ZZ^*$, etc. It was emphasized that the TD is favored by the current data thanks to the presence of extra technifermion loop corrections to digluon and diphoton couplings.

This talk summarizes the 125 GeV TD phenomenology at the LHC and shows a theoretically interesting possibility that the TD can indeed be as light as the 125 GeV boson by certain nontrivial feature intrinsic to the dynamics of WTC. The stability of the TD mass is also discussed, where it turns out that the large TD decay constant plays an important role against corrections from the SM particles in a low-energy region to be relevant after the walking behavior.

We start with a review of the characteristic features of WTC including the spontaneous breaking of both chiral and scale symmetries and the mass generation of TD (Sec. 2). We then discuss the size of the TD mass following two approaches: straightforward nonperturbative computations in the ladder approximation\textsuperscript{8–10} (Sec. 2.1) and a model estimate in a view of holography applied to WTC\textsuperscript{7,11} (Sec. 2.2). In contrast to the ladder estimate, the holographic model incorporates effects from the technigluon condensation, which turns out to play the crucial role to realize the TD mass on the order of 125 GeV.\textsuperscript{7}

To make direct contact with the LHC study, we derive a low-energy effective Lagrangian\textsuperscript{6} obtained by integrating out technifermions, which is governed by the lightest technihadron spectra involving the TD (Sec. 3). The Lagrangian is constructed based on nonlinear realization of the scale symmetry as well as the chiral symmetry coupled to the SM particles via the SM gauge interactions.

The TD couplings to the SM particles are read off from the effective Lagrangian. We then find that the couplings take essentially the same form as those of the SM particles, except two distinguishable ingredients: the overall scale of the couplings are set by the TD decay constant ($F_\phi$) associated with the spontaneous breaking of the scale symmetry, not by the electroweak (EW) scale ($v_{EW}$). Actually, $F_\phi$ turns out to be larger than $v_{EW}$ from both ladder and holographic estimates. The other crucial discrepancy comes in the couplings to diphoton and digluon, which get effects from technifermion loop contributions to be either enhanced or suppressed, depending on models of WTC. To be concrete, we will take one-family model for the WTC to explicitly calculate those couplings. After understanding the TD coupling property from the effective Lagrangian, we pay attention to the stability of the TD mass against radiative corrections arising from the SM particle loops. The large TD decay constant $F_\phi$ then turns out to play the crucial role to keep the TD mass around 125 GeV without invoking heavy fine tunning, in contrast to the SM Higgs case.

Finally, we shall explore the LHC production and decay processes of the 125 GeV TD in the one-family model and estimate the signal strengths for the relevant
channels to be compared with the experimental data on the Higgs searches (Sec. 4). It is shown that the TD signal is consistent with the currently reported data and can give a better fit than the SM Higgs, notably due to the presence of extra technifermion loop corrections.

2. Walking Technicolor and Technidilaton
Technicolor (TC)\textsuperscript{12,13} accommodates the EW symmetry breaking by technifermion condensation, without invoking the fundamental Higgs boson, just like the quark condensation in QCD, and hence gives the dynamical explanation for the origin of mass. The original version of TC,\textsuperscript{12} a naive scale-up version of QCD, was ruled out due to the excessive flavor-changing neutral currents.

A way out of this problem was suggested under a simple assumption of the existence of a large anomalous dimension for technifermion bilinear operator $\gamma_m$ without any concrete dynamics and concrete value of the anomalous dimension.\textsuperscript{14} It was the WTC\textsuperscript{3,4} that exhibited a concrete dynamics based on a nonperturbative analysis of ladder Schwinger-Dyson (SD) equation with nonrunning (scale invariant/conformal) gauge coupling, $\alpha(p) \equiv \alpha$, yielding a concrete value of the anomalous dimension, $\gamma_m = 1$ in the chiral broken phase. Modern version of WTC\textsuperscript{15–17} is based on the two-loop running coupling with the Caswell-Banks-Zaks infrared fixed point,\textsuperscript{18} instead of the nonrunning one, in the improved ladder SD equation.

Another problem of the TC as a QCD scale-up is the EW constraints, so-called $S$ and $T$ parameters. This may also be improved in the WTC.\textsuperscript{9,19} Even if WTC in isolation cannot overcome this problem, there still exist a possibility that the problem may be resolved in the combined dynamical system including the SM fermion mass generation such as the extended TC (ETC) dynamics,\textsuperscript{20} in much the same way as the solution (“ideal fermion delocalization”)\textsuperscript{21} in the Higgsless models which simultaneously adjust $S$ and $T$ parameters by incorporating the SM fermion mass profile.

It would be better to understand the WTC through an illustration by the notion of gauge dynamics: Figure 1 shows a schematic view of the WTC in terms of the gauge coupling $\alpha$ (left panel) and its beta function $\beta(\alpha)$ (right panel). In a field theoretical sense, the “walking” can be realized by an accidental balance between gluonic and fermionic contributions to the running of gauge coupling of $SU(N_{TC})$ gauge theory including $N_{TF}$ fermions. In fact, the presence of walking region implies a pseudo infrared fixed point ($\alpha_s$), a la Caswell-Banks-Zaks infrared fixed point based on the two-loop beta function in the large $N_f$ QCD.\textsuperscript{18} During the walking region (region II in Fig. 1), the gauge coupling slowly reaches the critical coupling, which is slightly off from an infrared fixed point $\alpha_s$, $\alpha_{cr}(< \alpha_s)$, where the chiral symmetry is dynamically broken by technifermion condensation $\langle \bar{F}F \rangle \neq 0$ and hence technifermions get the dynamical mass $m_F = \mathcal{O}(4\pi F_\pi) \sim 1$ TeV, where $F_\pi$ denotes the technipion decay constant associated with the chiral symmetry breaking. The walking regime (region II) expands in a wide range ($m_F < \mu < \Lambda_{TC}$): below
the infrared scale $m_F(\sim 1\text{ TeV})$, technifermions decouple and hence the balance with technigluon contributions gets lost, leading to the one edge of walking (region III), while above the ultraviolet scale $\Lambda_{TC}(\sim 10^3 - 10^4\text{ TeV})$ the theory will be embedded into an ETC (region I).

The dynamical mass generation of technifermion is characterized by so-called Miransky scaling,\textsuperscript{22} tied with the conformal phase transition,\textsuperscript{17}

$$m_F \sim \Lambda_{TC} e^{-\sqrt{\pi/\alpha_{cr}-1}}, \quad \text{for} \quad \alpha > \alpha_{cr}. \quad (1)$$

Note that this scaling property implies the wide-range walking regime above $\alpha_{cr}$ in region II of Fig. 1. The chiral condensate $\langle \bar{F}F \rangle$ is generated to scale with the large anomalous dimension $\gamma_m \simeq 1$ which solves the flavor-changing neutral current problem:\textsuperscript{3}

$$\langle \bar{F}F \rangle_{\Lambda_{TC}} \sim \frac{N_{TC}}{4\pi^2} m_F \Lambda_{TC}^2, \quad \langle \bar{F}F \rangle_{\Lambda_{TC}} \simeq \left( \frac{\Lambda_{TC}}{m_F} \right)^{\gamma_m \simeq 1} \langle \bar{F}F \rangle_{m_F}. \quad (2)$$

Of particular interest is the fact that the WTC possesses the (approximate) scale invariance $\langle \beta(\alpha) \rangle \simeq 0$ for $m_F < \mu < \Lambda_{TC}$, which is spontaneously broken by the technifermion condensation/mass generation. This implies presence of a (pseudo) Nambu-Goldstone boson (“dilaton”) for the scale symmetry. This is a flavor-singlet composite scalar and may be a mixture of $\bar{F}F$ bound state and techniglueball. That is the TD, technidilaton.

The TD gets massive essentially due to the “nonperturbative” scale anomaly: According to the dynamical mass generation in Eq.(1), the gauge coupling $\alpha$ is renormalized, starts running and hence the “nonperturbative” beta function $\beta_{NP}(\alpha)$ is generated:\textsuperscript{23}

$$\beta_{NP}(\alpha) = \Lambda_{TC} \frac{\partial \alpha}{\partial \Lambda_{TC}} = -\frac{2\alpha_{cr}}{\pi} \left( \frac{\alpha}{\alpha_{cr}} - 1 \right)^{3/2}. \quad (3)$$

This induces the “nonperturbative” scale anomaly:

$$\partial_\mu D^\mu = \frac{\beta_{NP}(\alpha)}{4\alpha^2} (\alpha G^2_{\mu\nu}) \neq 0, \quad (4)$$

where $D_\mu$ denotes the dilatation current and $G_{\mu\nu}$ the field strength of technigluon field. Thus the TD becomes massive due to the nonperturbative scale anomaly.\textsuperscript{3,4}
2.1. Technidilaton Mass: Ladder Estimate

A straightforward calculation based on the ladder SD equation and the ladder (homogeneous) Bethe-Salpeter (BS) equation in the walking regime indicates a relatively light scalar bound state (identified with TD):

\[ M_\phi \sim 4F_\pi \simeq 500 \text{ GeV}, \]  

(5)

for the one-family model with \( F_\pi \simeq 123 \text{ GeV} \). This \( M_\phi \) is much smaller than masses of the techni-vector/axial-vector mesons on TeV range, but still larger than the LHC boson at 125 GeV. This result is consistent with another calculation based on the ladder SD equation and the ladder (inhomogeneous) BS equation, and also consistent with other indirect computation based on the ladder gauged Nambu-Jona-Lasinio model.

In fact, the PCDC (partially conserved dilatation current) relation evaluated in the ladder approximation does not allow a very light TD unless the TD gets decoupled with divergent decay constant \( F_\phi \):

\[ F_\phi^2 M_\phi^2 = -4\langle \theta_\mu^\mu \rangle = \frac{\beta(\alpha)}{\alpha} \langle G_{\mu\nu}^2 \rangle, \]  

(6)

where \( \theta_\mu^\mu \) is the trace of energy-momentum tensor. To this relation, the ladder estimate gives \( F_\phi^2 M_\phi^2 \simeq 3\eta m_F^4 \) (near the conformal window) with \( \eta \simeq \frac{N_{TC}N_{TF}}{2\pi^2} = \mathcal{O}(1) \). This simply implies that the limit \( M_\phi/m_F \rightarrow 0 \), where the TD gets light compared with the weak scale \( m_F(=\mathcal{O}(4\pi F_\pi)) \), can only be realized when \( F_\phi/m_F \rightarrow \infty \), i.e., a decoupled limit:

\[ \text{Ladder : } \frac{M_\phi}{F_\pi} \rightarrow 0 \quad \text{only when} \quad \frac{F_\phi}{F_\pi} \rightarrow \infty. \]  

(7)

2.2. Technidilaton Mass: Holographic Estimate

As suggested earlier, however, there is a potential problem in the ladder approximation about the mass of the TD. Actually, the ladder approximation totally ignores non-ladder dynamics, say, most notably the full gluonic dynamics. Thus a possible way out would be to include fully nonperturbative gluonic dynamics. (Also a direct estimate of \( F_\phi \) free from the ladder approximation and without invoking the PCDC (without referring to \( M_\phi \)) is necessary to give more implications of the TD at the LHC.) One such a possibility besides lattice simulations would be a holographic computation based on the gauge-gravity duality.

We shall work on a recently proposed holographic model, which is based on deformation of a bottom-up approach for successful holographic-dual of QCD. The model describes a five-dimensional gauge theory having \( SU(N_{TF})_L \times SU(N_{TF})_R \) gauge symmetry, defined on the five-dimensional anti-de-Sitter space with the fifth direction being compactified on a finite interval. In addition to a bulk scalar dual to the technifermion bilinear operator \( \bar{F}F \) with the anomalous dimension \( \gamma_m = 1 \),
an extra bulk scalar field dual to technigluon condensate $\langle \alpha G^2_{\mu\nu} \rangle$ is incorporated \footnote{The extra bulk scalar dual to $\langle \alpha G^2_{\mu\nu} \rangle$ is actually necessary to properly reproduce the high energy behavior of vector/axial-vector current correlator including the gluon condensate term as predicted in the operator product expansion.}. 

Following the well-known holographic recipe, one can easily calculate the scalar (or dilatation) current correlator and examine the lowest pole identified as the TD mass to get a formula in a light TD limit:

$$M_\phi \sim \sqrt{\frac{3}{N_{TC}} \frac{\sqrt{3}/2}{1 + G}}, \quad \text{where} \quad G \sim \frac{\langle \alpha G^2_{\mu\nu} \rangle}{F_\pi^2}. \quad (8)$$

(The details can be found in the published paper.) This implies that, in contrast to the ladder approximation Eq.(5), the TD can be as light as the 125 GeV boson by a large gluonic effect $G$:

$$M_\phi \sim 125 \text{ GeV} \quad \text{at} \quad G \simeq 10, \quad (9)$$

for the one-family model with $N_{TC} = 3$. It is also interesting to note that the gluonic effect in QCD is much smaller, $G|_{QCD} \simeq 0.25$.\footnote{The extra bulk scalar dual to $\langle \alpha G^2_{\mu\nu} \rangle$ is actually necessary to properly reproduce the high energy behavior of vector/axial-vector current correlator including the gluon condensate term as predicted in the operator product expansion.}\footnote{The extra bulk scalar dual to $\langle \alpha G^2_{\mu\nu} \rangle$ is actually necessary to properly reproduce the high energy behavior of vector/axial-vector current correlator including the gluon condensate term as predicted in the operator product expansion.}

Similarly, one can calculate the TD decay constant $F_\phi$ by examining the pole residue of the dilatation current correlator to find a formula:

$$F_\phi \approx \sqrt{2N_{TF}}. \quad (10)$$

This and Eq.(8) indicate that, in contrast to the ladder approximation Eq.(7), a very light/massless TD with the finite decay constant $F_\phi$ can be realized when $G$ goes to infinity:

$$M_\phi \rightarrow 0 \quad \text{and} \quad \frac{F_\phi}{F_\pi} = \text{constant}, \quad \text{as} \quad G \rightarrow \infty. \quad (11)$$

The large $G$ limit actually corresponds to a “conformal” limit where $\beta(\alpha) \rightarrow 0$: Combining Eqs.(8) and (10) with the PCDC relation in Eq.(6) and calculating the technigluon condensate $\langle \alpha G^2_{\mu\nu} \rangle$, one can evaluate the beta function as a function of $G$ to find that $\beta(\alpha) \sim \frac{1}{G(1 + G)^2} \rightarrow 0$ as $G \rightarrow \infty$\footnote{The extra bulk scalar dual to $\langle \alpha G^2_{\mu\nu} \rangle$ is actually necessary to properly reproduce the high energy behavior of vector/axial-vector current correlator including the gluon condensate term as predicted in the operator product expansion.}.

Thus the holographic estimate suggests that a very light TD with the finite decay constant can be allowed due to the conformality tied with the nonperturbative gluonic effect $G$.

Though this holographic result is strong enough to indicate the presence of the 125 GeV TD, we would anticipate that lattice simulations will give a more conclusive answer.

3. Low-Energy Effective Lagrangian

Below the technifermion mass scale $m_F = O(4\pi F_\pi) \sim 1$ TeV (See region III in Fig. 1), the WTC can be viewed as an effective technihadron model as in the QCD case. Such an effective model will be described by a low-energy effective Lagrangian based on nonlinear realization of both chiral and scale symmetries, involving the
125 GeV TD and the SM particles, which is most relevant for the LHC study. The chiral/EW and scale invariant Lagrangian thus takes the form:

\[ \mathcal{L}_{\text{inv}} = \frac{v_{\text{EW}}^2}{4} \chi^2 \text{tr}[D_\mu U^\dagger D^\mu U] + \mathcal{L}_{\text{kin}}(\chi), \]

where \( \chi = e^{\phi/F_{\phi}} \) is a nonlinear base of the scale symmetry, which parametrizes the TD field \( \phi \) with the decay constant \( F_{\phi} \) and has the scale dimension 1; \( D_\mu U = \partial_\mu U - i W_\mu U + i U B_\mu \) with the \( SU(2)_W \) and \( U(1)_Y \) gauge fields \( W \) and \( B \); \( \mathcal{L}_{\text{kin}}(\chi) \) denotes the scale invariant kinetic term of TD and \( U \) the usual chiral field parameterizing the (eaten) Nambu-Goldstone boson fields \( \pi \) as \( U = e^{2i \pi/v_{\text{EW}}} \); The \( |D_\mu U|^2 \) term gives the TD couplings to massive weak bosons:

\[ g_{\phi WW/ZZ} = \frac{2m_{W/Z}^2}{F_{\phi}}. \]

As seen in Eqs.(3) and (4), the scale symmetry is actually broken explicitly as well as spontaneously by dynamical mass generation of technifermions, which has to be respected also in the nonlinear realization. Such explicit breaking effects arise in the TD Yukawa couplings to the SM fermions, which reflect underlying ETC-induced four-fermion terms, and couplings to QCD gluons and photons related to the scale anomaly in the SM gauge sector. In order to incorporate these effects into the scale-invariant Lagrangian, we introduce a spurion field \( S \) having the scale dimension 1 coupled to the SM fermions, digluon \( gg \) and diphoton \( \gamma\gamma \) in such a way that:

\[ \mathcal{L}_S = -m_f \left( \left( \frac{\chi}{S} \right)^{2-\gamma_m} \cdot \chi \right) \bar{f} f + \log \left( \frac{\chi}{S} \right) \left\{ \frac{\beta_F(g_s)}{2g_s} G_{\mu\nu}^2 + \frac{\beta_F(e)}{2e} F_{\mu\nu}^2 \right\}, \]

where \( G_{\mu\nu} \) and \( F_{\mu\nu} \) respectively denote the field strengths for QCD gluon and photon fields; \( g_s \) and \( e \) are the QCD gauge and electromagnetic couplings, respectively; \( \beta_F \)s are the beta functions only including the technifermion loop contributions.

The TD Yukawa coupling to the SM \( f \)-fermion arises from the first line of Eq.(14) as

\[ g_{\phi ff} = \frac{(3-\gamma_m)m_f}{F_{\phi}}, \]

along with scale dimension of technifermion bilinear operator \( (3-\gamma_m) \). The anomalous dimension \( \gamma_m \approx 1 \) in WTC, which is crucial to obtain the realistic mass of the SM fermions of the first and the second generations without suffering from the flavor-changing neutral current problems. However it was known for long time that it is not enough for the mass of the third-generation SM \( f \)-fermions like \( t, b, \tau \): A

\[ ^b \text{We focus only on the TD phenomenology with the SM particles and disregard technipions, some of which might participate in the low-energy model as discussed in a recent paper.} \]
simplest resolution would be the strong ETC model\textsuperscript{31} having much larger anomalous dimension \( 1 < \gamma_m < 2 \) due to the strong effective four-fermion coupling from the ETC dynamics in addition to the walking gauge coupling. Here we take \( \gamma_m \simeq 2 \), i.e., \( (3 - \gamma_m) \simeq 1 \), as in the strong ETC model for the third-generation SM \( f \)-fermions like \( t, b, \tau \) which are relevant to the current LHC data.

3.1. Technidilaton Couplings to the SM particles

We see from Eqs.(13) and (15) that the TD couplings to \( W \) and \( Z \) bosons and fermions are related to those of the SM Higgs by a simple scaling:

\[
\frac{g_{\phi WW/ZZ}}{g_{hSM WW/ZZ}} = \frac{v_{EW}}{F_{\phi}}, \quad \frac{g_{\phi ff}}{g_{hSM ff}} = \frac{v_{EW}}{F_{\phi}}, \quad \text{for} \quad f = t, b, \tau. \tag{16}
\]

In addition to the above scaling, the couplings to gluon and photon (\( G_{\mu\nu}^{2} \) and \( F_{\mu\nu}^{2} \) terms in Eq.(14)) involve the beta functions, \( \beta_{F}(g_{s}) \) and \( \beta_{F}(\epsilon) \), induced from \( F \)-technifermion loops.\textsuperscript{5} We shall employ the one-family model as a concrete WTC setting and evaluate the betas \( \beta_{F}(g_{s}) \) and \( \beta_{F}(\epsilon) \) at the one-loop level in the perturbation:\textsuperscript{c}

\[
\text{one-family model:} \quad \beta_{F}(g_{s}) = \frac{g_{s}^{3}}{(4\pi)^{2}} \frac{4}{3} N_{TC}, \quad \beta_{F}(\epsilon) = \frac{e^{3}}{(4\pi)^{2}} \frac{16}{9} N_{TC}. \tag{17}
\]

We thus find the scaling from the SM Higgs for the couplings to \( gg \) and \( \gamma\gamma \), which can approximately be expressed at around 125 GeV as

\[
\text{one-family model:} \quad \frac{g_{hSM gg}}{g_{SM gg}} \simeq \frac{v_{EW}}{F_{\phi}} \cdot (1 + 2 N_{TC}) \quad \text{and} \quad \frac{g_{hSM \gamma\gamma}}{g_{SM \gamma\gamma}} \simeq \frac{v_{EW}}{F_{\phi}} \cdot (1 - \frac{32}{47} N_{TC}), \tag{18}
\]

where in estimating the SM contributions we have incorporated only the top and \( W \) boson loop contributions.

One could actually derive these TD couplings directly from the Ward-Takahashi identities for the dilatation symmetry (low-energy theorem).\textsuperscript{6}

As seen from Eqs.(16) and (18), once the ratio \( v_{EW}/F_{\phi} \) is fixed, the TD LHC phenomenological study can be made just by quoting the SM Higgs coupling properties: We may estimate \( F_{\phi} \) based on the ladder approximation:\textsuperscript{9} The TD decay constant \( F_{\phi} \) can actually be related to the TD mass \( M_{\phi} \) through the PCDC – which is analogous to the PCAC (partially conserved axialvector current) relation for the QCD pion – involving the vacuum energy density \( \mathcal{E}_{\text{vac}} \):

\[
F_{\phi}^{2} M_{\phi}^{2} = -16 \mathcal{E}_{\text{vac}}. \tag{19}
\]

\textsuperscript{c}This one-loop approximation can be justified in ladder estimate of the scale anomaly-related vertices \( \phi\gamma(g)\gamma(g) \).\textsuperscript{6}
The vacuum energy density \( \mathcal{E}_{\text{vac}} \) is saturated by the technigluon condensation induced from the technifermion condensation, so is generically expressed as

\[
\mathcal{E}_{\text{vac}} = -\kappa_V \left( \frac{N_{TC} N_{TF}}{8\pi^2} \right) m_F^4 ,
\]

where \( m_F \) denotes the dynamical technifermion mass and \( N_{TF} = 2N_D + N_{EW-singlet} \) with \( N_D \) being the number of EW doublets formed by technifermions and the number of dummy technifermions, \( N_{EW-singlet} \), which are singlet under the SM gauges. The overall coefficient \( \kappa_V \) is determined once a straightforward nonperturbative calculation is made. The dynamical technifermion mass \( m_F \) can, on the other hand, be related to the technipion decay constant \( F_\pi \):

\[
F_\pi^2 = \kappa_F^2 \frac{N_{TC}^4}{4\pi^2} m_F^2 ,
\]

with the overall coefficient \( \kappa_F \) and the property of \( N_{TC} \) scaling taken into account. The values of \( \kappa_V \) and \( \kappa_F \) may be quoted from the latest result\(^{24} \) on a ladder Schwinger-Dyson analysis for a modern version of WTC:\(^{15-17} \)

\[
\kappa_V \simeq 0.7 \quad \text{and} \quad \kappa_F \simeq 1.4 ,
\]

where \( \kappa_F \) has been estimated based on the Pagels-Stokar formula.\(^{32} \) In that case \( N_{TF} \) is fixed by the criticality condition for the walking regime as\(^{16} \)

\[
\frac{N_{TF}}{4N_{TC}} \simeq 1 .
\]

The estimated values in Eqs.(22) and (23) are based on ladder approximation which are subject to certain uncertainties up to 30\% observed for the critical coupling and hadron spectrum in QCD.\(^{33} \) We may include this 30\% uncertainty in estimation of each independent factor \( \kappa_V , \kappa_F^2 \) and the criticality condition \( N_{TF}/(4N_{TC}) \). Putting these all together, we thus estimate \( v_{EW}/F_\phi \) as

\[
\text{one-family model : } \left. \frac{v_{EW}}{F_\phi} \right|_{\text{Ladder}} \simeq (0.1 - 0.3) \times \left( \frac{N_D}{4} \right) \left( \frac{M_\phi}{125 \text{ GeV}} \right) ,
\]

(24)

Alternatively, using the holographic estimate in Eq.(10) and incorporating a typical ~30\% correction into the holography coming from the next-to-leading order terms in \( 1/N_{TC} \) expansion, we may estimate the TD decay constant \( F_\phi \) to get\(^{7} \)

\[
\text{one-family model : } \left. \frac{v_{EW}}{F_\phi} \right|_{\text{holo}} ^{+1/N_{TC}} \simeq 0.2 - 0.4 .
\]

(25)

which is coincidentally consistent with the ladder estimate in Eq.(24). Note that the two calculations are quite different qualitatively in a sense that the ladder calculation has no massless TD limit, while the holographic model including the nonperturbative gluonic dynamics does. Nevertheless, such a numerical coincidence may suggest that both models are reflecting some reality through similar dynamical effects for the particular mass region of the 125 GeV TD.
3.2. Technidilaton Mass Stability

Before proceeding to the LHC phenomenology, we shall briefly remark on stability
of the light TD mass against radiative corrections. As a pseudo Nambu-Goldstone
boson of scale invariance, the quadratic divergence is suppressed by the scale in-
variance for the walking regime \( m_F < \mu < \Lambda_{\text{TC}} (\sim \Lambda_{\text{ETC}}) \) (region II in Fig. 1). The
scale symmetry breaking in the ultraviolet region \( \mu > \Lambda_{\text{TC}} \) (region I in Fig. 1) has
no problem thanks to the naturalness as usual like in the QCD and the QCD-scale-
up TC where the theory has only logarithmic divergences. Only possible source of
the scale symmetry violation is from an effective theory for \( \mu < m_F \) (region III in
Fig. 1).

Below \( \mu = m_F \) the dominant corrections to the TD mass \( M_\phi \) come from the SM
top quark loop \(^4\), which can be estimated from the effective Lagrangian in Eqs.(12)
and (14) as

\[
\delta M_\phi^2 \simeq -\frac{3}{4\pi^2} \frac{m_t^2}{F_\phi^2} m_F^2 ,
\]

where the cutoff has been set by \( m_F \). Due to the large TD decay constant \( F_\phi \sim
1 \text{TeV} (\sim m_F = \mathcal{O}(4\pi F_\phi)) \) (see Eq.(25)), this correction only gives a tiny shift to the
125 GeV TD mass (Note numerically \( m_t^2 \simeq 2M_\phi^2 \)):

\[
\left| \frac{\delta M_\phi}{M_\phi(125 \text{GeV})} \right| \simeq \frac{3}{4\pi^2} \frac{m_t^2}{F_\phi^2} \simeq \mathcal{O}(10^{-2} - 10^{-1}) .
\]

Thus the 125 GeV TD mass is fully stable against the radiative corrections, in
contrast to the unnatural SM Higgs case.

4. 125 GeV Technidilaton Signal at the LHC

We now discuss the 125 GeV TD phenomenology at the LHC based on the coupling
properties derived in the previous section. As is clear from Eqs.(16) and (25), the
TD couplings to the SM particles are simply suppressed by the large decay constant
\( F_\phi \) compared to the SM Higgs case. As seen from Eq.(18), however, the gluon-gluon
fusion (ggF) and diphoton couplings can be enhanced due to extra contributions
from technifermions in the one-family model which compensate the overall sup-
pression by \( F_\phi \). Thus the ggF process becomes mostly dominant in the TD LHC
production, while other production processes such as vector boson fusion (VBF)
and vector boson associate production (VH) are suppressed simply by the large TD
deay constant \( F_\phi \). Similarly, the branching fraction is almost governed by the decay
to digluon which becomes comparable with \( b\bar{b} \) channel for the SM Higgs, while other
channels such as the decay to \( WW^* \), \( ZZ^* \) and fermion pairs are suppressed. (The

\(^4\)Actually, a TD potential term involving the usual \( \lambda \phi^4 \) coupling could yield a similar correction to
\( M_\phi \) at one-loop level. This contribution, however, turns out to be negligible in magnitude compared
to the top-loop correction in Eq.(26), due to the high suppression factor \((M_\phi/(4\pi F_\phi))^2\). \(^6\)
TD total width at 125 GeV is comparable with the SM Higgs one.) More details on the production and decay properties can be found in the published papers.6

In order to make a direct comparison with the current LHC data,1,2,34 we estimate the TD signal strengths normalized to the SM Higgs cross section,

$$\mu_X = \frac{\sigma_\phi(pp \to \phi) \times \text{BR}(\phi \to X)}{\sigma_{h_{\text{SM}}}(pp \to h_{\text{SM}}) \times \text{BR}(h_{\text{SM}} \to X)}.$$  \hfill (28)

Taking the one-family model with $N_{\text{TC}} = 4$ and $v_{\text{EW}}/F_\phi = 0.2$ as a benchmark, in Table 1 we summarize the predicted signal strengths at 125 GeV for each category relevant to the current Higgs search at 8TeV LHC. As for VBF-tag categories, we have taken into account about 30% contamination from the ggF process as in the case of the SM Higgs.

| channel          | ggF-tag | VBF-tag | VH-tag |
|------------------|---------|---------|--------|
| $\gamma\gamma$   | 1.4     | 0.4     | 0.02   |
| $ZZ^*$           | 1.0     | 0.3     | 0.01   |
| $WW^*$           | 1.0     | 0.3     | 0.01   |
| $\tau^+\tau^-$  | 1.0     | 0.3     | 0.01   |
| $b\bar{b}$       | —       | —       | 0.01   |

From Table 1 we see that the diphoton signal strength for the ggF-tag category is slightly enhanced and can explain the currently reported excess at the LHC,1,2,34 while other channels in the ggF-tag categories are almost SM Higgs-like, not distinguishable from those for the SM Higgs. The characteristic feature of the 125 GeV TD in the one-family model is seen at the VBF- and VH-tag categories, which are significantly suppressed compared to the SM Higgs case, simply due to the overall suppression of the couplings by the large decay constant $F_\phi$. This will be tested in the future, though the presently observed significance on such categories are still lower than those for the ggF-tag category.

Finally, we shall test the goodness-of-fit of the TD with use of the current LHC data,1,2,34 based on the $\chi^2$ function:

$$\chi^2 = \sum_{i \in \text{events}} \left( \frac{\mu_i - \mu_i^\text{exp}}{\sigma_i} \right)^2,$$  \hfill (29)

where $\mu_i^\text{exp}$ denote the best-fit strengths for each channel reported and $\sigma_i$ the corresponding one sigma errors. Taking $(v_{\text{EW}}/F_\phi)$ as a free parameter so as to satisfy the theoretically expected range in Eq.(24) (or Eq.(25)), in Fig. 2 we plot the $\chi^2$ function for the 125 GeV TD in the one-family model with $N_{\text{TC}} = 3, 4, 5$. In particular, the best-fit values for $N_{\text{TC}} = 4, 5$ are as follows:

| $N_{\text{TC}}$ | $(v_{\text{EW}}/F_\phi)_{\text{best}}$ | $\chi^2_{\text{min}}$/d.o.f |
|-----------------|---------------------------------|-----------------------------|
| 4               | 0.22                            | 18/19 ≃ 0.95               |
| 5               | 0.17                            | 18/19 ≃ 0.95               |
which are compared with the SM Higgs case, $\chi^2_{\text{SM}} \simeq 33/20 \simeq 1.6$, implying that the TD is more favorable than the SM Higgs ($\mu_i = 1$). This nice goodness of fit is due to the significant enhancement in the diphoton channel coming from the sector beyond the SM (technifermions): The technifermion loop contributions as in Eq.(18) become large enough to compensate the smallness of the overall $(v_{EW}/F_\phi)$ in Eq.(24).

5. Conclusion

The TD is the characteristic light composite scalar in WTC. The mass can be 125 GeV, protected by the approximate scale invariance. The TD mass is also stable
against the SM radiative corrections, where the large TD decay constant plays an important role. The couplings to the SM particles take essentially the same form as those for the SM Higgs, except couplings to diphoton and digluon which involve a high model-dependence. The 125 GeV TD in the one-family model gives the LHC signal consistent with the LHC data, notably can explain the currently reported diphoton excess. More precise measurements in VBF and VH categories will draw a definite conclusion that the TD is favored, or not.

Note added:

After the SCGT 12 workshop, the ATLAS and CMS have reported updated data in some channels for the Higgs search involving $WW^*, ZZ^*, \tau^+\tau^-$ and diphoton channels.\textsuperscript{35,36} However, the signals in VBF- and VH-tag categories have not yet clearly been measured, which would actually be the most characteristic for the 125 GeV TD in the one-family model: The most significant channels with the significance over $\sim 3 - 4$ sigma are still only in the ggF-tag categories, as far as the amount of observed excess over the background is concerned. See Table 2. Thus the 125 GeV TD in the one-family model is still consistent with the latest data. Further update on measurements in the VBF- and VH-tag categories is needed to more definitely say that is the TD, or not.

| category   | TD signal strength | ATLAS significance | CMS significance |
|------------|--------------------|--------------------|------------------|
| ggF-tag    |                    |                    |                  |
| $\mu_{gg}$ | 1.4                | 1.6 ± 0.4          | ~ 6σ             |
| $\mu_{WW}$ | 1.0                | 0.8 ± 0.4          | ~ 4σ             |
| $\mu_{ZZ}$ | 1.0                | 1.8 ± 0.5          | ~ 6σ             |
| $\mu_{\gamma\gamma}$ | 1.0 | 2.1 ± 0.5 | < 2σ |
| VBF-tag    |                    |                    |                  |
| $\mu_{\nu\nu}$ | 0.4 | 1.7 ± 0.9 | < 2σ with VH |
| $\mu_{WW}$ | 0.3                | 1.7 ± 0.8          | < 2σ             |
| $\mu_{ZZ}$ | 0.3                | 1.2 ± 0.4          | < 2σ with VH    |
| $\mu_{\gamma\gamma}$ | 0.3 | −0.4 ± 0.0 | < 2σ with VH |
| VH-tag     |                    |                    |                  |
| $\mu_{VH}$ | 0.02               | 1.8 ± 1.9          | < 2σ with VBF   |
| $\mu_{\nu\nu}$ | 0.01 | — | — |
| $\mu_{WW}$ | 0.01               | 1.2 ± 1.4          | < 2σ with VBF   |
| $\mu_{ZZ}$ | 0.01               | −0.4 ± 1.0         | < 2σ with VBF   |
| $\mu_{\gamma\gamma}$ | 0.01 | −0.4 ± 1.0 | < 2σ |
| $\mu_{\nu\nu}$ | 0.01 | −0.4 ± 0.4 | < 2σ with VBF |
| $\mu_{WW}$ | 0.01               | 1.8 ± 0.9          | < 2σ with VBF   |
| $\mu_{ZZ}$ | 0.01               | −0.4 ± 0.4         | < 2σ with VBF   |
| $\mu_{\gamma\gamma}$ | 0.01 | 1.8 ± 1.0 | < 2σ |

Table 2. The predicted 8TeV LHC signal strengths of 125 GeV TD in the one-family model with $N_{TC} = 4$ and $v_{EW}/F_0 = 0.2$ fixed, in comparison with the latest LHC data as of Moriond 2013 EW and QCD sessions (or Aspen 2013-Higgs Quo Vadis) in 2013.\textsuperscript{35,36} The sizes of the observed significance for signal over background have also been displayed.
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