High-Temperature Deformation Behaviors of the C-Doped and N-Doped High Entropy Alloys

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Abstract: High entropy alloys (HEAs) containing multi-principal metallic constituents have attracted much attention. A good understanding of their hot-deformation behavior and recrystallization mechanism is the prerequisite for microstructures tuning and for optimizing mechanical performance. Here, the flow behavior and recrystallization mechanism of the N-doped and C-doped face-centered cubic phase HEAs are produced at high temperatures by hot-compression at 1123–1273 K, with strain rates of 0.1–0.001 s⁻¹. Constitutive equations were successfully constructed to reveal flow behavior, and stress-strain curves were predicted using strain compensated polynomial functions. Discontinuous and continuous dynamic recrystallization proceeded concurrently when compressed at a low temperature and high strain rate, whereas discontinuous recrystallization, which occurs at primary grain boundaries, became predominant at a high temperature and low strain rate, significantly contributing to the refinement and homogenization of the grains. For this reason, a relatively high temperature and a low strain rate, in which the recrystallized grains exhibit equiaxed morphology and very weak texture, are more suitable for refining grains. The average size of the grains was approximately 10 µm. This study sheds light on grain optimization and mechanical properties through thermomechanical processing.

Keywords: high entropy alloys; interstitial strengthening; hot deformation; recrystallization; constitutive equation; grain structure

1. Introduction

Conventional alloys for load-bearing applications are generally designed based on one host metal with the minor addition of other alloying elements to optimize the microstructure and mechanical properties. The concept of high entropy alloys (HEAs) was first proposed in the year 2004 and broadened the realm of possibility for developing novel high-performance metallic materials [1,2]. HEAs contain more than four principal elements, where the atomic percentage of each element is between 5 at% and 35 at% [1,2]. Hereinto, the face-centered cubic (FCC) single-phase CoCrFeMnNi HEA, known as Cantor alloy, is one of the most promising candidates. The Cantor HEA shows an unprecedented combination of strength and ductility as well as excellent fracture toughness, particularly at cryogenic temperatures [2–5]. This exceptional mechanical performance is attributed to its low stacking fault energy (SFE, 25–30 mJ/m²) [6]. The SFE plays a crucially important role in the regulation of plastic deformation behavior and mechanical performance: a high SFE value (>45 mJ/m²) results in dislocation slip and the formation of dislocation cells during deformation; an intermediate SFE value (15–45 mJ/m²) promotes the activation of deformation twinning, which increases strength and ductility in a process known as twinning-induced plasticity (TWIP); a low SFE value (<15 mJ/m²) stimulates the strain-induced displacive phase transformation from an FCC structure to an HCP (hexagonal close-packed) structure, which elevates the strength and ductility because of
the transformation-induced plasticity (TRIP) effect [7–12]. For this reason, the Cantor HEA exhibits high strength and large ductility with the assistance of the TWIP effect.

Furthermore, the CoCrNi medium entropy alloy (MEA), a derivative of the Cantor alloy, was proposed soon afterward, which exhibits a further enhanced mechanical performance due to its reduced SFE (18 m J/m$^2$) [6]. As mentioned above, it is reasonable to optimize the mechanical properties of HEAs and MEAs by regulating the SFE. For this purpose, guidelines for regulating SFE in the Cantor, CoCrFeNi, and CoCrNi alloys have been recently proposed and use the combinatorial methods of first-principle calculations, thermodynamic predictions, and experimental verifications [8–10]. The results showed that an increase in the content of Co and Cr at the expense of Mn, Ni, and Fe in the Cantor alloy significantly reduces the SFE [9]. Similarly, the SFE and the stability of the FCC phase decrease when the Co concentration increases, but this also decreases the Fe and Ni concentrations; meanwhile, the elastic modulus, anisotropy, and lattice friction force increased as well [8]. Further, a minor addition of Mo could increase the lattice constant and decrease the SFE and elastic modulus [10]. Based on these findings, a series of novel high-performance Co-rich non-equiatomic HEAs and MEAs were developed and exhibit tensile properties that are superior to other reported FCC single-phase HEAs or MEAs. The Co-rich HEAs/MEAs show an enhanced strain hardening behavior, which can be attributed to either the TWIP effect or the FCC $\rightarrow$ HCP TRIP effect [8–10]. Although hardening is improved, the yield strength of those alloys still needs to be elevated.

One of the more promising strategies is to introduce interstitial non-metal atoms (C, N, O) into the solid solutions of the metals, benefiting from the interstitial solid-solution strengthening and/or the short-range order/ordered complexes [13–17]. Moreover, the yield strength could also be further enhanced by reducing the grain size, wherein fine grains result in a high yield strength, which is known as the Hall–Petch relation [18,19]. Nevertheless, cold processing is not appropriate for alloys with the TRIP effect due to the poor workability of the deformation-induced HCP-phase. For this reason, thermomechanical processing, which has been devoted to producing excellent products with precious dimensions and optimal mechanical properties, is an alternative candidate for refining the grain structures of hard materials [20–23]. In this process, the grains are refined by dynamic recrystallization (DRX) and/or static recrystallization (SRX) [20]. Deep insight into the hot-deformation mechanism, the microstructure evolution, and the DRX mechanism is a prerequisite for optimizing grain structures [20–23]. It was reported that discontinuous dynamic recrystallization (dDRX) notably contributed to grain refinement during hot-deformation, in which the recrystallized grains tend to nucleate at the primary grain boundaries (GBs) [14,24]. The apparent activation energy of the Cantor HEA is close to that of the diffusion of Ni in the alloy, and the dislocation climb determines the steady-state deformation [25–32]. Even though the DRX behaviors of CoCrNi MEA and the novel Co-rich TRIP HEA were investigated in our previous studies [14,24], the influence of interstitial atoms such as C and N on hot-deformation and grain structure evolution have not been clarified.

In the present study, we aimed to reveal the microstructure evolution, grain refinement, hot-deformation of C-doped and N-doped HEAs/MEAs by conducting hot-compression tests at various conditions and by constructing the corresponding constitutive relationships. The present study will shed light on the thermomechanical processing of interstitial solid-solution strengthened HEAs and MEAs in order to optimize grain structure and mechanical properties.

2. Materials and Methods

In the present study, the quaternary TRIP-HEA with a nominal composition of Co$_{45}$Cr$_{25}$Fe$_{15}$Ni$_{15}$ (at.%) was selected as the base-alloy, and the alloy was then doped with 0.1 wt.% C and 0.05% wt.% N. Ingots of the C-doped HEA and the N-doped HEA with a diameter of 50 mm were prepared by vacuum induction melting and casting. The as-casted ingots were forged at 1473 K to a cross-section of 30 $\times$ 30 mm$^2$. Additionally, the forged
samples were then homogenized at 1473 K for 24 h followed by water quenching to room temperature. The chemical composition of the two HEAs was Co$_{44.41}$Cr$_{23.7}$Fe$_{14.5}$Ni$_{17.3}$C$_{0.09}$ (wt.%) for the C-doped HEA and Co$_{44.55}$Cr$_{23.605}$Fe$_{14.6}$Ni$_{17.2}$N$_{0.045}$ (wt.%) for the N-doped HEA, which are close to the nominal compositions. Cylindrical specimens with a dimension of 8 mm (diameter) × 12 mm (height) were sliced from the ingots by means of electric discharge machining. The hot-deformation mechanism and the DRX behavior of the HEAs were measured by means of hot-compression tests using a Gleeble 1500 machine (Dynamic systems Inc., Poestenkill, New York, USA). During hot-compression, the temperature was monitored by thermocouples, and the friction between the specimens and anvils was minimized by using two thin mica foils. The compression was conducted under an Ar gas atmosphere.

The experimental procedure of the hot-compression used in this research is schematically illustrated in Figure 1. The specimens were first heated up to 1473 K and held for 300 s for homogenization and were then cooled to the compression temperatures of 1123 K, 1173 K, 1223 K, and 1273 K at a cooling rate of 10 K/s. Each specimen was held at the desired temperature for 10 s before compression. After that, the specimens were compressed to a 63% reduction in height (an equivalent true strain of 1.0) at a strain rate of 0.1 s$^{-1}$, 0.01 s$^{-1}$, and 0.001 s$^{-1}$. The compressed specimens were water-quenched immediately to room temperature within 15 s. More than three independent tests were repeated for each compression condition.

![Figure 1. The schematic diagram demonstrating the procedure for hot-compression tests of the C-doped and N-doped TRIP HEAs.](image)

The microstructures of the hot-deformed specimens were characterized using a scanning electron microscope (SEM, Hitachi S-3400N, HITACHI, Tokyo, Japan) equipped with an electron backscatter diffraction (EBSD, OIM Analysis, AMETEK Inc., Berwyn, PA, USA) detector. An acceleration voltage of 20 kV was used for the observations. In the present study, the hot-deformed cylindrical specimens were sliced vertically through the center in a direction parallel to the loading axis. Then, the central regions were observed using SEM-EBSD. The surface of the specimens was polished with abrasive paper and were mirror-finished using a colloidal silica suspension (OP-U).

3. Results
3.1. Flow Behaviors during Hot-Compression

Figures 2 and 3 show the compressive stress-strain (S-S) curves of the N-doped HEA (Figure 2) and the C-doped HEA (Figure 3) compressed at (a) 1123 K, (b) 1173 K, (c) 1223 K, and (d) 1273 K with the strain rates of 0.1 s$^{-1}$, 0.01 s$^{-1}$, and 0.001 s$^{-1}$, respectively. All of the S–S curves exhibit an analogous trend, in which the flow stress increases rapidly with the increase of strain at the initial stage of compression (hardening stage), and then the flow stress decreases with the increase of strain (softening stage) after a stress peak. At the hardening stage, the dislocation density increases with the increase of strain because the
multiplication rate and dislocations storage are higher than those of the dynamic dislocation recovery. The forest of dislocations formed in the early stage inhibits the nucleation and motion of new dislocation, thus increasing the flow stress for further deformation until reaching a peak value. After the peak, the flow softening with the increase of strain can mainly be attributed to the dynamic recovery (DRV) of dislocations and/or DRX. The discontinuous yield behavior frequently reported in many HCP metals is not observed in the present FCC-phase HEAs [21–23]. On the other hand, the value of the peak flow stress tends to be increased by decreasing the temperature and/or by increasing the strain rate. It is because the multiplication of the dislocations competes with the DRV of the dislocations [20]. By decreasing the temperature and/or by increasing the strain rate, the DRV is inhibited because of the low mobility at a low temperature and the less time that is available for their recovery at a high strain rate. This leads to a high density of stored dislocations (high peak stress). In contrast, the DRV of the dislocations becomes more preferred by increasing the temperature (higher mobility of dislocations) and/or by decreasing the strain rate (longer time for recovery), which leads to reduced work hardening and a small peak stress value. It should be noted that the sharpened drops of the flow stress (Figure 3c,d) in the C-doped HEA were not observed in the N-doped HEA (Figure 2a–d).

![Figure 2. True stress-strain curves of the N-doped HEA compressed at (a) 1123 K, (b) 1173 K, (c) 1223 K, and (d) 1273 K. The strain rates were 0.1 s⁻¹, 0.01 s⁻¹, and 0.001 s⁻¹.](image-url)
where the log function on both sides of Equations (1)-(3), the expressions become as follows:

\[ \ln \dot{\varepsilon} = \ln A_1 + n_1 \ln \sigma - \frac{Q_{\text{def}}}{RT} \] (4)

\[ \ln \dot{\varepsilon} = \ln A_2 + \beta \sigma - \frac{Q_{\text{def}}}{RT} \] (5)

\[ \ln n \dot{\varepsilon} = \ln A + n \ln[\sinh(\alpha \sigma)] - \frac{Q_{\text{def}}}{RT} \] (6)

According to Equations (4)-(6), the value of \( a \) is calculated as 0.00581. Additionally, the values of \( n \) and \( Q_{\text{def}} \) can then be calculated as follows:

\[ n = \left\langle \frac{\partial \ln \dot{\varepsilon}}{\partial (\sinh(\alpha \sigma))} \right\rangle_T \] (7)

**Figure 3.** True stress-strain curves of the C-doped HEA compressed at (a) 1123 K, (b) 1173 K, (c) 1223 K, and (d) 1273 K. The strain rates were 0.1 s\(^{-1}\), 0.01 s\(^{-1}\), and 0.001 s\(^{-1}\).

### 3.2. Constitutive Analysis

During hot deformation, the flow stress is affected by the temperature, strain rate, and strain. The correlation among these parameters can be expressed by using an appropriate constitutive equation. Here, the well-known Arrhenius type hyperbolic-sine relationship equations were used, which were first proposed by Sellars and Tegart [33–36]:

\[ \dot{\varepsilon} = A_1 \sigma^{n_1} \exp\left(-\frac{Q_{\text{def}}}{RT}\right) (\alpha \sigma < 0.8) \] (1)

\[ \dot{\varepsilon} = A_2 \exp(\beta \sigma) \exp\left(-\frac{Q_{\text{def}}}{RT}\right) (\alpha \sigma > 1.2) \] (2)

\[ \dot{\varepsilon} = A [\sinh(\alpha \sigma)]^n \exp\left(-\frac{Q_{\text{def}}}{RT}\right) \text{ (for all)} \] (3)

where \( \dot{\varepsilon} \) is the strain rate (s\(^{-1}\)); \( A_1, A_2, A, \alpha (=\beta / n_1), \beta, n_1, \) and \( n \) are material constants; \( \sigma \) is the flow stress (MPa); \( Q_{\text{def}} \) is the apparent activation energy for high-temperature deformation (J·mol\(^{-1}\)); \( R \) is the gas constant (8.314 J·K\(^{-1}\)·mol\(^{-1}\)); and \( T \) is the compression temperature (K). Equation (1) is suitable for low stress, and Equation (2) is applied for high stress. However, Equation (3) can be applied for all the deformation conditions. By taking the log function on both sides of Equations (1)–(3), the expressions become as follows:
\[ Q_{\text{def}} = nR \langle \partial (\sinh (a \sigma)) / \partial (1/T) \rangle \varepsilon \] (8)

The values of the \( \ln(\varepsilon) \) and \( \ln[\sinh(a\sigma)] \) at various temperatures are plotted and linearly fitted in Figure 4a, in which the average value of the slopes (n) was measured to be 4.69. Furthermore, the relationship between the value of \( \ln[\sinh(a\sigma)] \) and \( 1000/T \) is described in Figure 4b, in which the value of \( Q_{\text{def}} \) was determined to be 334685 J/mol.

\[ \varepsilon_{\text{def}} = 1.97 \times 10^{20} \sinh(0.00581\sigma) \exp\left[-\frac{526078}{RT}\right] \] (12)

On the other hand, the temperature-compensated \( \dot{\varepsilon} \) can be expressed by the simple Zener–Hollomon parameter (Z) [37,38]:

\[ Z = \dot{\varepsilon} \exp \left( \frac{Q_{\text{def}}}{RT} \right) \] (9)

By comparing Equations (3) and (9) and by taking the log function on both sides, we achieve

\[ \ln Z = \ln A + n \ln[\sinh(a\sigma)] \] (10)

The correlation between the values of \( \ln Z \) and \( \ln[\sinh(a\sigma)] \) is plotted and linearly fitted, as shown in Figure 4c. The fitting coefficient is 0.983, which reveals a significant linear dependence. Additionally, the value of A was then determined to be \( 1.42 \times 10^{12} \). Finally, the constitutive relationship, which describes the hot deformation behavior of the N-doped HEA at a temperature of 1123–1273 K and a strain rate of 0.001–0.1 s\(^{-1}\), is as follows:

\[ \dot{\varepsilon} = 1.42 \times 10^{12} \sinh(0.005290\sigma) \exp\left(\frac{-334685}{RT}\right) \] (11)

Moreover, we utilized the same procedure to determine the value of \( n, Q_{\text{def}}, \) and A for the C-doped HEA, as demonstrated in Figure 5. After careful plotting and linear-fitting, the average value of the slopes (n) was measured to be 5.72 (Figure 5a). The correlation of the \( \ln[\sinh(a\sigma)] \) and \( 1000/T \) at different strain rates was plotted and linearly fitted as shown in Figure 5b. The value of \( Q_{\text{def}} \) was measured to be 526078 J/mol. The linear fitting coefficient between the \( \ln Z \) and \( \ln[\sinh(a\sigma)] \) is 0.983, which also demonstrates an obvious linear dependence. The value of A was calculated to be \( 1.97 \times 10^{20} \). Eventually, the constitutive relationship, which describes the hot-deformation behavior of the C-doped HEA, can be expressed as follows:

\[ \dot{\varepsilon} = 1.97 \times 10^{20} \sinh(0.00581\sigma) \exp\left(\frac{-526078}{RT}\right) \] (12)

**Figure 4.** The correlation of the values of the (a) \( \ln \) and \( \ln[\sinh(a\sigma)] \), (b) \( \ln[\sinh(a\sigma)] \) and \( 1000/T \), and (c) \( \ln Z \) and \( \ln[\sinh(a\sigma)] \) of the N-doped HEA, which was compressed at 1123 K, 1173 K, 1223 K, and 1273 K. The strain rates were 0.1 s\(^{-1}\), 0.01 s\(^{-1}\), and 0.001 s\(^{-1}\). The correlations demonstrated in Figure 4a–c, are linearly fitted.
The values of the $\ln(\dot{\varepsilon}_\text{ref})$ and $\ln[\sinh(\alpha \dot{\varepsilon})]$ at various temperatures and $1000/T$ are linearly fitted in Figure 4a, in which the average value of the slopes ($n$) was measured to be 5.72 (Figure 5a). The correlation demonstrated in Equations (3) and (9) and by taking the log function on both sides, we can achieve $\ln Z$ and $\ln[\sinh(\alpha \dot{\varepsilon})]$ of the C-doped HEA, which was compressed at 1123 K, 1173 K, 1223 K, and 1273 K. The strain rate is 0.1 s$^{-1}$.

To verify the accuracy of the constructed constitutive models with strain compensation, the experimentally measured flow stress and the predicted flow stress at a wide range of strains were plotted and compared in Figure 6. Figure 6a shows the comparison of the
S–S curves of the N-doped HEA at 1123 K and the various strain rates of N-doped HEA, while Figure 6b compares the S–S curves at a strain rate of 0.001 s⁻¹ and a temperature of 1123 K, 1173 K, 1223 K, and 1273 K. Figure 6c,d demonstrate the comparison of the S–S curves of the C-doped HEA under the same conditions as described in Figure 6a,b. All of the results indicate that the constitutive model efficiently predicted the flow stress over the entire range of conditions. The majority of the predicted values lie fairly close to the best regression line, in which the square correlation coefficients \( R^2 = \frac{\sum_{i=1}^{n} (\sigma'_i - \sigma_i)(\sigma'_i - \sigma_i)}{\sum_{i=1}^{n} (\sigma'_i - \bar{\sigma})(\sigma'_i - \bar{\sigma})} \) are 0.981 for the N-doped HEA and 0.994 for the C-doped HEA, indicating a good agreement of the predicted and experimental data. The \( \sigma_c \) and \( \sigma_p \) represent the experimentally measured value and the predicted value obtained from the constitutive models. The \( \bar{\sigma} \) and \( \bar{\sigma}_p \) are the mean value of the \( \sigma_c \) and \( \sigma_p \). Moreover, the average absolute relative errors \( (\text{AARE}) = \frac{1}{n} \sum_{i=1}^{n} \frac{|\sigma'_i - \sigma_i|}{\sigma'_i} \) between the predicted and measured values for the entire range of deformation parameters is 4.49% (N-doped HEA) and 5.97% (C-doped HEA), respectively. Therefore, one can conclude that our developed constitutive model can effectively predict the high-temperature flow behavior of both the N-doped HEA and the C-doped HEA.

Figure 6. Comparison of experimentally measured results and the modally predicated (dotted) for the N-doped HEA (a,b) compressed at (a) 1123 K with various strain rates and (b) at a strain rate of 0.001 s⁻¹ under various temperatures. (c,d) The comparison for the C-doped HEA under conditions that are the same as those in (a,b).

3.3. Microstructure after Hot Compression

Figure 7 shows the EBSD image quality (IQ) maps of the N-doped HEAs compressed at 1123 K (a–c), 1173 K (d–f), 1223 K (g–i), and 1273 K (j–l), respectively. The blue lines in the maps illustrate the high-angle grain boundaries (HAGBs) with a misorientation angle larger than 15°; meanwhile, the red lines show the low-angle grain boundaries (LAGBs) with misorientation angles of 2°–15°. When the HEA was compressed at a low temperature and/or at a high strain rate (Figure 7a–d,f,i,l), very fine grains were formed at the GBs of the primary coarse grains. Those fine grains were formed via dDRX, which forms a necklace structure with the primary coarse grains [27]. Further, the primary grains were elongated...
towards the metal flow direction, and then a large number of deformation-induced LAGBs were formed in the interior of the primary grains. This indicates that partial DRX at the GBs and the plastic deformation of primary grains proceeded at these compression conditions. However, a much larger fraction of the DRXed grains with both an equiaxed shape and fine size were obtained when the HEA was compressed at a higher temperature and/or lower strain rate (Figure 7g,j,k). The majority of the DRXed grains were enclosed by HAGBs, and annealing twins were frequently observed within the DRX grains due to the low SFE. In contrast, the fraction of LAGBs is very low at these conditions.

![EBSD image quality (IQ) maps of the N-doped HEA compressed at 1123 K (a–c), 1173 K (d–f), 1223 K (g–i), and 1273 K (j–l) with strain rates of 0.001 s\(^{-1}\) (a,d,g,j), 0.01 s\(^{-1}\) (b,e,h,k), and 0.1 s\(^{-1}\) (c,f,i,l), respectively.](image)

Figure 7. EBSD image quality (IQ) maps of the N-doped HEA compressed at 1123 K (a–c), 1173 K (d–f), 1223 K (g–i), and 1273 K (j–l) with strain rates of 0.001 s\(^{-1}\) (a,d,g,j), 0.01 s\(^{-1}\) (b,e,h,k), and 0.1 s\(^{-1}\) (c,f,i,l), respectively.

Figure 8 shows the EBSD inverse pole figure (IPF) maps of the C-doped HEA compressed at 1123 K (a–c), 1173 K (d–f), 1223 K (g–i), and 1273 K (j–l) with strain rates of 0.001 s\(^{-1}\) (a,d,g,j), 0.01 s\(^{-1}\) (b,e,h,k), and 0.1 s\(^{-1}\) (c,f,i,l), respectively. The colors in the IPF maps demonstrate the crystal orientation of the grains. It can be seen that the necklace structure consisting of coarse-grain and fine-DRXed grains prefer to form at lower temperatures and/or at higher strain rates (Figure 8a–f,i,l), which is consistent with what can be seen in the IQ maps. The DRX leads to flow softening (a decrease in flow stress with the increase of strain) in the S–S curves in Figure 2. Let us note that the DRXed grains do not
exhibit a particular orientation relationship with their adjacent coarse grains. The grain structures were further homogenized and refined with the increase of the temperature and the decrease of the strain rate (Figure 8g,h), in which a larger number of DRXed-grains were produced. This shows that a high temperature with a low strain rate is the optimum condition for obtaining a homogenized grain structure.

Figure 8. EBSD IQ maps of the N-doped HEA compressed at 1123 K (a–c), 1173 K (d–f), 1223 K (g–i), and 1273 K (j–l) with strain rates of 0.001 s$^{-1}$ (a,d,g,j), 0.01 s$^{-1}$ (b,e,h,k), and 0.1 s$^{-1}$ (c,f,i,l), respectively.

Figure 9 shows the EBSD IQ maps of the C-doped HEA compressed at 1123 K (a–c), 1173 K (d–f), 1223 K (g–i), and 1273 K (j–l) and at strain rates of 0.001 s$^{-1}$ (a,d,g,j), 0.01 s$^{-1}$ (b,e,h,k), and 0.1 s$^{-1}$ (c,f,i,l), respectively. The corresponding EBSD IPF maps are shown in Figure 10. Compared to the results of the N-doped specimens, the following similarities can be drawn: (i) a necklace structure revealing partial DRX behavior is observed in both of the samples, which is more preferred at lower temperatures and/or at higher strain rates; (ii) the fine grains in the necklace structure are DRXed grains, which are preferentially formed in the vicinities of the primary grain boundaries, and the fine DRXed grains are enclosed by HAGBs; (iii) the DRXed grains have no preferential orientation, exhibiting very weak texture. However, some differences can also be found between the two HEAs as follows: (i) a higher fraction of the DRXed grains tend to be formed in the C-doped HEA...
than in the N-doped HEA after compression in the same conditions; (ii) the grain size of
the two samples is different, which will be further discussed in the upcoming section.

Figure 9. EBSD IQ maps of the C-doped HEA compressed at 1123 K (a–c), 1173 K (d–f), 1223 K (g–i), and 1273 K (j–l) with strain rates of 0.001 s\(^{-1}\) (a,d,g,j), 0.01 s\(^{-1}\) (b,e,h,k), and 0.1 s\(^{-1}\) (c,f,i,l), respectively.
Figure 10. EBSD IPF maps of the C-doped HEA compressed at 1123 K (a–c), 1173 K (d–f), 1223 K (g–i), and 1273 K (j–l) with strain rates of 0.001 s\(^{-1}\) (a,d,g,j), 0.01 s\(^{-1}\) (b,e,h,k), and 0.1 s\(^{-1}\) (c,f,i,l), respectively.

4. Discussion

In the present study, the mechanical response and microstructure evolution of the N-doped and the C-doped Co\(_{45}\)Cr\(_{25}\)Fe\(_{15}\)Ni\(_{15}\) (at.%\) TRIP HEA were investigated. The compressive S–S curves exhibited analogous behavior, in which the flow stress increased with the increased strain at the initial stage up to a flow stress peak due to work hardening, and then the flow stress decreased with the increase of strain attributed to DRX. The observations of the microstructure also demonstrate that DRX preferred to occur at the GBs of the primary grains, forming a necklace structure when the compression was conducted at low temperatures and/or high strain rates. However, homogeneous DRXed grain structures with a refined grain size were produced when the HEAs were compressed at a high temperature and low strain rate.

For single-phase FCC metals, the SFE is a crucially important factor that affects the hot-deformation and DRX mechanisms. In high SFE metals (>160 mJ/m\(^2\)), the DRV of the dislocations is preferred to proceed by climbing and cross-slipping [20,41]. The compressive S–S curves often exhibit the following characteristics: strain hardening at a small strain up to a plateau (peak stress), and flow stress is then almost constant even though the strain increases successively [42,43]. In this case, DRX almost does not occur because of the lack of dislocations, which is the prerequisite driving force for the occurrence
of DRX, and subgrains with LAGBs are formed due to dislocation multiplication and their DRV [44–47]. However, the DRV is significantly inhibited by the reduction of the SFE. In pure Ni and Cu with an SFE lower than 90 mJ/m², DRX occurs after hot-deformation to a critical strain [48–50]. The equiatomic CoCrFeNi HEA has an SFE of 25–30 mJ/m² [6], which is much lower than that of the Ni and Cu. Further, our previous ab initio calculation and thermodynamic predictions revealed that the increase of Co content at the expense of Fe and Ni could notably reduce the SFE of the HEA [8–10]. For this reason, the SFE of the Co₄₅Cr₂₅Fe₁₅Ni₁₅ (at.%) TRIP HEA and the C-doped or N-doped derivates is below 25 mJ/m². The HEAs investigated in the present study exhibited obvious flow softening due to DRX, as indicated in Figures 2 and 3.

The apparent activation energies for the hot-deformation of the N-doped and the C-doped HEAs are 334.7 kJ/mol and 526.1 kJ/mol, respectively. The activation energies of pure Ni, Cu, and Al are 285 kJ/mol, 197 kJ/mol, and 142 kJ/mol, respectively [30,31]. We know that the activation energy of the HEA is much larger than that of pure metals, which indicates the sluggish diffusion of elements in the HEAs containing multi-principal elements. This sluggish diffusion leads to a reduction of the DRV and postpones the occurrence of DRV; as a result, the flow stress of the HEA is higher than that of the pure metals. Moreover, the activation energy of the C-doped HEAs is much larger than that of the N-coped counterpart because a larger amount of C (0.09 wt.%) than what is found in N (0.045 wt.%) was successfully doped in the system. One can deduce that the activation energy of the HEAs would be increased by doping interstitial atoms, and a larger amount of doping yields higher activation energy.

Apart from the SFE and activation energy, the compression condition (temperature and strain rate) also exerted a strong influence on the flow behaviors and microstructure evolutions, as demonstrated in Figures 2, 3 and 7–10. For a better comparison, the volume fraction of the recrystallized grains and their average size were measured, and the recrystallized grains were distinguished by using a grain orientation spread (GOS) method [51,52]. The grains with a GOS ≤ 2° were determined to be recrystallized grains, and the grains with a GOS > 2° were un-recrystallized ones. Figure 11a,b displays the recrystallization fraction (Figure 11a) and the average size of the recrystallized grains (Figure 11b) of the N-doped HEA. It can be seen that the volume fraction of the DRXed grains increases when the temperature increases and/or the strain rate decreases. For instance, the volume fraction is 16.3% when compressed at 1123 K with 0.01 s⁻¹, but it increases to 86.3% when compressed at 1273 K with 0.001 s⁻¹. An obviously increasing recrystallization fraction could be observed when the alloy was compressed at temperatures between 1173 K and 1223 K with a certain strain rate of 0.001 s⁻¹. The average grain size of the recrystallized grains increases when the temperature increases or when the strain rate decreases. A fine crystallized grain size of about 10 µm or less can be obtained in most conditions except for when being compressed at 1273 K with 0.001 s⁻¹. Therefore, a high temperature of 1223 K and a low strain rate of 0.001 s⁻¹ is an appropriate condition for obtaining a large amount of recrystallized structures with a small grain size.
In the present study, the flow behavior and the grain structure evolutions of 0.045 wt.% N-doped and 0.09 at.% C-doped Co_{45}Cr_{25}Fe_{15}Ni_{15} (at.%) TRIP-HEAs were investigated by hot-compression at 1123, 1273, 1223, and 1473 K up to a true strain of 1.0. The influence of the compression temperature and strain rate (0.1, 0.01, and 0.001 s\(^{-1}\)) was clarified. Based on the results, the following conclusions can be drawn:

1. Constitutive equations for combing the flow behaviors and compression conditions were constructed successfully. The hyperbolic-sine of stress has a linear relationship with the Zener–Hollomon parameter. Further, the flow stresses were predicted and fitted using fifth-order polynomial functions. The apparent activation energies of the N-doped and C-doped HEAs are 334.7 kJ/mol and 526.1 kJ/mol, respectively. The larger activation energy than that of the pure metals indicates sluggish diffusion in the HEAs.

2. The stress-strain curves exhibited strain hardening (flow stress increases with strain) at a small strain up to the peak of flow stress, and then the curves exhibited flow softening (flow stress decreases with the increase of strain). The low SFE of the HEAs promoted softening (flow stress decreases with the increase of strain). The low SFE of the HEAs promoted
the storage of dislocations, i.e., strain hardening, while the dynamic recrystallization occurring preferentially at the grain boundaries of the primary grains contributed to the flow softening.

3. The recrystallized grain structure was significantly influenced by the compression conditions. A higher fraction of recrystallized grains were produced when the HEAs were compressed at a relatively high temperature and/or low strain rate. A temperature of 1223 K and a strain rate of 0.001 s⁻¹ is optimal for obtaining homogeneous grain structures for the N-doped HEA, while the optimum conditions for the C-doped HEA are 1173–1273 K with a strain rate of 0.001 s⁻¹. The average size of the recrystallized grains is approximately 10 μm, and no obvious texture is observed.

Author Contributions: Conceptualization, D.W.; methodology, H.Y. and D.W.; validation, H.Y. and D.W.; formal analysis, H.Y., Y.Z., R.X., M.B. and D.W.; investigation, H.Y., Y.Z., R.X. and M.B.; resources, H.Y. and D.W.; data curation, H.Y. and D.W.; writing—original draft preparation, H.Y. and D.W.; writing—review and editing, D.W.; visualization, H.Y., R.X., Y.Z., M.B. and D.W.; supervision, H.Y.; project administration, H.Y. and D.W.; funding acquisition, H.Y. and D.W. All authors have read and agreed to the published version of the manuscript.

Funding: The authors gratefully appreciate the financial support provided by the National Natural Science Foundation of China (51674079) and the China Postdoctoral Science Foundation (2016M600211). This work was supported by Grant-in-Aid for Scientific Research from the Japan Society for the Promotion of Science (JSPS) KAKENHI (Grant No. 19K14838, 21K03766).

Data Availability Statement: All data in this study are available from the corresponding author upon reasonable request.

Acknowledgments: This work was partially supported by the “Creation of Life Innovation Materials for Interdisciplinary and International Researcher Development” project. This work is a cooperative program (Proposal No. 20G0420) of the Cooperative Research and Development Center for Advanced Materials, Institute for Materials Research, Tohoku University.

Conflicts of Interest: The authors declare no conflict of interest.

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