A COUPLED DIFFUSION-MECHANICAL LATTICE MODEL FOR THE DEGRADATION OF GRAPHITE ACTIVE PARTICLES OF LI-ION BATTERY ANODES

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Abstract. The performance and durability of lithium-ion batteries (LIBs) are constrained by the degradation mechanisms that take place during charge and discharge cycles. Degradation of active particles (APs) of LIBs is a complex problem involving several physical phenomena (e.g., diffusion, mechanical deformation, heat transfer, to cite a few). During lithium insertion and extraction cycles, volume changes in the AP result in high mechanical stresses and, consequently, mechanical damage that promotes capacity fade.

In this work, we present a microscale 3D finite element model that takes into account the coupled effects between lithium diffusion and mechanical stress within the AP. Using the surface of an ellipsoid as the base for the geometrical construction, we are able to generate different shapes of APs, with both concave and convex surfaces. Porosity and other types of defects that may be present inside the AP are explicitly modeled, and different volume fractions, shapes, and orientations are also accounted for. In our approach, the material is discretized into a lattice of one-dimensional elements: we consider beam elements for the mechanical problem, while in the diffusive approach, the material is treated as an assembly of “nanopipes” through which the flow of Li-ions takes place. The same lattice network is used for both simulations. We follow a classical lattice model approach to characterize the fracture behavior of a single AP of a LIB anode when subjected to charge/discharge cycles. The material of the APs analyzed in this work is graphite, which presents a brittle, disordered material structure, making it suitable for lattice modeling. The mechanical problem is solved, obtaining the crack patterns associated with specific charge and discharge strategies and potential initial defects.

The simulation results correctly reproduce the experimental observations on mechanical stresses and the evolution of damage. This lattice model framework analyzing the degradation in the APs of LIBs (durability) can be used to provide more information regarding the microstructural evolution, morphological changes, and mechanical degradation in APs and identify improvement strategies.

1 INTRODUCTION

Nowadays, one of the greatest challenges facing the electric power industry is how to deliver the energy in a useable form, as a higher-value product, especially in the area of renewable
energy. By storing the power produced and releasing it during peak demand periods, energy storage can transform power into a high-value product. Among the different possible choices, the electrochemical batteries are the most suitable energy storage systems: portable devices able to deliver the stored chemical energy, as electrical energy, with high conversion efficiency, and without emissions [1–3]. There is a large variety of applications: from consumer applications to electric vehicles, photovoltaics or large-size auxiliary energy supply. The main challenges of battery production are insufficient battery performance, unknown future demands, and cost pressure [4,5]. Within this context, some of the most important goals arise such as the improvement of battery performance and durability, scalability, reduction of production costs, and reduction of environmental impacts of batteries [6–8].

In this work, we have focused on lithium-ion batteries (LIB), which currently have one of the highest energy densities of any rechargeable battery technology. And more specifically, in the active particles (AP) of the anode.

The lifetime of batteries is conditioned by mechanisms of chemo-mechanical degradation, such as the formation of microcracks within the AP, due to diffusion-induced stress (DIS), or the formation of the solid-electrolyte interphase (SEI) [9,10]. It is of critical importance to understand these degradation mechanisms, which constrains battery life [11,12]. Fracture due to diffusion-induced stress of the electrode active particles has been identified as one of the critical factors for the capacity fade. In recent years, attention has been paid to this degradation mechanism [10,13–15]. Microcracks are formed when the intercalation-induced stress in the active particles exceeds the fracture limit of the material. The formation of cracks and their propagation through the particle leads to an increase in the formation of SEI and a consequent decrease in available Li-ions in the loading/unloading cycles. Determining the stress level within the AP is essential to be able to estimate the evolution of mechanical degradation.

Several studies have focused on stress generation and fracture in LIBs active particles. Christensen and Newman developed pioneering work on determining the distribution of mechanical stress within carbonaceous anode material [14]. They analyzed the effect of hydrostatic stress and volume expansion during Li-ion intercalation within spherical APs. Several particle sizes, lithium insertion rates, and external pressure were considered. Zhang et al. proposed a thermal analogy model to calculate DIS in spherical and ellipsoidal shape particles [16]. Cheng and Verbrugge presented analytical solutions to evaluate the stress within a spherical AP under galvanostatic or potentiostatic conditions [17]. Barai and Mukherjee presented a lattice spring-based numerical methodology to estimate the initiation, nucleation, and propagation of microcracks within graphite active particles. Their model permits obtaining the evolution of lithium concentration and successive mechanical degradation [18].

In most of the models that study degradation in APs, simple shapes (sphere, ellipsoids, or combinations of both) are usually considered. However, real particles have a multitude of convex and concave surfaces, which generate stress concentrations during cycles, where the fracture process is most likely to begin [19]. In this work, random APs are generated, in order to capture the effect of the geometric characteristics on intercalation stresses of particles which may lead to damage.

In this study, we have focused on graphite AP of LIB anodes. Graphite has traditionally been used as active material in the anode of LIBs. And today it is still used in most commercial LIBs, despite the continuous search for alternatives that could improve energy or power density, and at the same time, capable of maintaining good stability in dis/charge cycles. Several aspects
remain to be understood regarding the de/lithiation mechanism, the reactions occurring at the electrode/electrolyte interface, and the factors limiting the rapid intercalation of lithium-ions into the graphite.

This work aims at using numerical methods to analyze the mechanical degradation within the active particles of LIBs, for different porosity types and porosity ratios, and particle shapes. A numerical framework has been developed to capture the initiation and propagation of microstructural damage and its impact on the diffusion of Li-ions within active particles. This methodology is based on the lattice model, where the continuum is replaced by a lattice of beam elements. This kind of model was introduced to model the fracture processes in brittle materials such as cement paste, mortar, concrete, and rocks [20-21].

2 LATTICE MODEL FRAMEWORK

2.1 General formulation of the problem

Fracture due to diffusion-induced stress of electrode active particles has been investigated through numerical means, focused on the material level, at the microscale. We have set a framework to capture the initiation and propagation of damage within AP. Initially, the distribution of Li-ion concentration inside the particle is obtained by solving the diffusion equation modeling the transport of Li-ions inside graphite, as a single-phase diffusion process. Then, mechanical stress within the particle due to the contraction/expansion caused by the de/lithiation process is calculated. As a main assumption, mechanical damage is used to explain the degradation behavior of materials due to micro-damage, and it is coupled to the diffusive damage. In this work, we are not considering associated heat transfer phenomena.

The numerical framework used in this work is the so-called lattice model, a discrete modeling technique, which presents an alternative to continuum models for fracture analysis of brittle and disordered materials. The material subject of our study is graphite of electrode active particles, which is a brittle material appropriate to be analyzed using the lattice model.

2.2 Spatial discretization

In the lattice model, the domain is discretized by a network of beam elements, forming a lattice, whose nodes are placed as follows: the domain is divided into cubic cells and then, a sub-cell is defined inside each cell. A node is randomly placed in every sub-cell. The randomness of the mesh is defined by the ratio between the size of sub-cell and cell. Finally, a Delaunay tessellation of the set of nodes is performed to obtain the final lattice network.

It is important to assign the correct cross-sectional area of the lattice elements [22]. In this work, this value has been calibrated by fitting the simulation results to the analytical solution of a representative problem (i.e. expansion/contraction of a sphere subjected to external pressure).
In the mechanical lattice approach, in order to study the mechanical degradation of the AP, Euler-Bernoulli beam elements with shear correction are used. In the diffusive lattice approach, to analyze the diffusion of lithium inside the active particle, the material is treated as an assembly of one-dimensional “nanopipes”, through which the flow takes place. The diffusion of ions takes place within the solid medium. For this reason, the same lattice mesh for both simulations is used.

2.3 Generation of particles

Graphite active particles have been traditionally modeled as spherical-like particles. However, it is well known that the shape of the particle influences the global behavior of the material. In this work, we analyze the effect of the shape on the fracture properties. We are considering three types of shapes, which are the most representative, depending on the natural or synthetic origin of the graphite particles: spherical and two ellipsoidal shapes, one of them with a flaky shape (Figure 2a).

There are mesopores inside the Active Particles, that change the Li-ion transport mechanism, and diffusion induced stress. Porosity and other types of defects that may be present inside the AP are explicitly modeled to understand their effect on the diffusive and mechanical degradation process. In this case, we consider three types of porosity (Figure 2b):

1) Concentrated porosity defect.
2) Scattered porosity 1: microspheres.
3) Scattered porosity 2: microflakes.

In all these cases, with different volume fractions of pores (0, 2.5, 5, 7.5 and 10%).

In order to generate realistic shapes of APs, we use the surface of an ellipsoid as the base for the geometrical construction, to create random graphite APs. Several random points on the surface of the ellipsoid can be chosen as the vertices of the convex polyhedron (Figure 1 (c)):

\[
\begin{align*}
    x_i &= a \sin \varphi_i \cos \theta_i \\
    y_i &= b \sin \varphi_i \sin \theta_i \\
    z_i &= c \cos \varphi_i
\end{align*}
\]

being \(a\), \(b\) and \(c\) are the semiaxes of the wrapping ellipsoid, with angles:

\[
\begin{align*}
    \theta_i &= \frac{2\pi}{n} + \delta \frac{2\pi}{n} (2\eta - 1) \quad \forall i = 1, \ldots, n \\
    \varphi_i &= 2\pi \eta \quad \forall i = 1, \ldots, n
\end{align*}
\]

where \(\eta\) and \(\delta\) are random numbers between 0 and 1.
We consider polyhedra of 40 vertices in our numerical simulations.

2.4 Numerical Scheme

The numerical scheme in order to solve the coupled diffusive and mechanical problem is described in this section. For each time step: firstly, the diffusive problem is solved. Once the Li-ion concentration in the active particle has been calculated, diffusive forces applied to the lattice elements are obtained. Then, these element forces are applied to solve the mechanical problem. The damage parameter is computed, and, finally, the mechanical and diffusion matrices are updated.

**Diffusive problem**

The diffusion process in the active material is described as follows [15]:

\[
\frac{\partial c}{\partial t} = -\nabla \cdot \mathbf{J}
\]

where \( c \) represents the concentration of lithium ions in the AP and \( \mathbf{J} \) is the diffusion flux. For simplification, it is assumed that there is no of stress gradients effects on the lithium ions flux. According to Fick’s law, the diffusion flux is proportional to the concentration gradient:
where $D$ is the diffusion coefficient.

Combining Eqs. (3) and (4), and assuming a constant diffusion coefficient:

$$\frac{\partial c}{\partial t} = D \nabla^2 c$$

The initial boundary condition is:

$$c = c_0$$

And, at the outer boundary, we impose the species flux:

$$J = \frac{i_n}{F} n$$

where $i_n$ is the current density and $F$ is Faraday’s constant. The Butler-Volmer equation, establishes that the reaction current density on the electrode surfaces is a function of the exchange current density and the overpotential. In this study, we consider galvanostatic conditions instead.

**Mechanical problem**

The brittle damage constitutive model is used within the lattice model framework. This model describes degradation of a material due to micro-cracking with the aid of a single scalar damage parameter $d_m$, growing from zero (undamaged state) to one (completely damaged state).

The stress-strain relationship is represented by the Eq. (8):

$$\sigma = (1 - d_m) D_{0} e^d$$

$$e^d = e - e^d$$

$$e^d = c \Omega I$$

where $D_0$ is the stiffness tensor, $e = \epsilon - c_0$ is the change in the Li-ion concentration from the initial value (stress-free status), and $\Omega$ is the partial molar volume of the active material.

Failure criterion requires the comparative stress in the lattice beam element is smaller than its strength. The lattice beam element stress (note it is a scalar) is computed by Eq. (11) from internal forces applying beam theory. If it is greater than the maximum allowable tensile stress, the mechanical damage $d_m$ is set to 1.

$$\sigma_{eq-\text{lattice beam}} = \alpha_N F \frac{A}{A} + \alpha_M \frac{(M_1, M_2)_{\text{max}}}{W}$$

where, for each lattice beam element, $F$ is the axial force in the lattice beam element, $A$ is the cross-sectional area of the element, $M_1$ and $M_2$ are the bending moments, $W$ is the cross-sectional modulus for bending resistance, and $\alpha_N$ and $\alpha_M$ are the normal force and the bending influence factor in the fracture criterion. Typical values are $\alpha_N = 1$ and $\alpha_M = 0$.

To describe the evolution of the diffusive damage parameter, a power law could be assumed, as well as other types of laws that are adjusted according to experimental results.

Stiffness matrix updates following Eqs (12):

$$K_m = (1 - d_m) K_{m,0}$$

where $K_{m,0}$ is the undamaged stiffness matrix.
3 RESULTS

Different particle shapes (shape 1: sphere, R= 5 µm; shape 2: ellipsoid, semi-axes: a>b=c, \(V_{\text{ellipsoid}}=V_{\text{sphere}}\); shape 3: ellipsoid, semi-axes: a>b>c, \(V_{\text{ellipsoid}}=V_{\text{sphere}}\)), different porosity types (one concentrated defect; scattered porosity 1: microspheres; scattered porosity 2: microflakes), and porosity ratios (0, 2.5, 5, 7.5 and 10%) were analyzed to study their effects on the fracture behavior of the active particle. The material properties of graphite used in the simulations are listed in Table 1. For simplification, \(E\), \(\nu\), \(D\) of graphite is assumed to remain constant.

| Property                               | Unit             | Li\(_2\)C\(_6\) | Reference |
|----------------------------------------|------------------|-----------------|-----------|
| Young’s module (E)                     | GPa              | 15              | [23]      |
| Poisson’s ratio (\(\nu\))             |                  | 0.3             | [23]      |
| Diffusion coefficient (D)              | m\(^2\)·s\(^{-1}\) | 7.08 x 10\(^{-15}\) | [23] |
| Partial molar volume (\(\Omega\))      | m\(^3\)·mol\(^{-1}\) | 3.60 x 10\(^{-6}\) | [23] |
| Maximum Li-ion concentration (c\(_{\text{max}}\)) | mol·m\(^{-3}\) | 2.29 x 10\(^{4}\) | [23] |
| Maximum allowable tensile stress (MPa) | MPa              | 87.5            | [24]      |

3.1 Diffusive Problem

Figure 3 shows the results of lithium-ion concentration during lithiation, at different time steps. In this first simulation, no mechanical damage is considered. The particle is spherical, with no porosity. It can be seen that the surface of the particle exhibits the higher lithium-ion concentration, whereas the inner area exhibited lower concentration. The concentration profile evolves as the simulation progresses smoothing the concentration gradient within the particle.

Applying these concentration results, the diffusion-induced stress due to Li insertion (during charge) is computed at different time steps. The outer region of the active particle expands as Li-ions are inserted, producing a strain difference between the outer and the inner regions of the particle. As result, the stress (normal stress in the lattice element) during the lithiation is tensile at the center of the particle, but compressive at the surface, due to the expansion during lithium insertion. Maximum tensile stress value at the center of the particle increases over time.
In the opposite way, diffusion-induced stress due to Li extraction (during discharge) is computed at different time steps. In the opposite way to the previous case, during the delithiation, the stress is compressive at the center of the particle, but tensile at the surface. The maximum value of stress is located at the center of the particle (Fig. 4b).
Figure 5: Mechanical damage during lithiation at different time steps, spherical shape, porosity 0-10%. Porosity type: (a) one concentrated defect; (b) scattered porosity 1: microspheres; (c) scattered porosity 2: microflakes

Figure 6 shows the mechanical damage distribution in case of ellipsoidal shape and flake
shape. Porosity types are compared at the same time steps. It can be seen that the microcracks are more localized in spherical shape than in the ellipsoidal one. Less localized microcracks patterns are observed in shape 3.

**Figure 6**: Mechanical damage during lithiation at different time steps. (a) Shape 2: ellipsoid. (b) Shape 3: flake. Porosity type: 1, 2, 3.

### 4 CONCLUSIONS

In this work we have presented a novel approach to the characterization of active particles performance in Li-ion battery anodes. In our approach, we are able to generate 3D virtual
microstructures that not only take into account different geometrical aspects of the particles (e.g., shape, convexity), but also allows the inclusion of inter- and intragranular defects. These microstructures are then subject to diffusion and mechanical analyses to understand better the role of imperfections in the degradations of this type of particles.

For the simulation of the physical phenomena (ion diffusion and deformation), we have used a 3D lattice model, consisting of 1D elements that represent the internal microstructure of the material. In the diffusion problems, these elements are equivalent to “nanopipes” through which Li ions transport through the material, while in the case of the mechanical problems, are beams that represent the mechanical interaction between different points in the material. This approach also allows for the simulation of crack initiation and propagation. In this sense, the mechanical damage variable is used to explain the degradation behavior of graphite due to micro-damage, and it is coupled to the diffusive damage.

The results obtained with our model are in accordance with the literature, especially in the mechanical stress distribution and evolution of damage.

Future works include coupling this material-level simulation to the characterize their behavior in components (i.e., electrodes) through a multiscale.

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