Metal-insulator transition
induced by fluctuations of the magnetic potential
in semiconductors with magnetic impurities

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We investigate the metal-insulator transition occurring in semiconductors with magnetic impurities when lowering temperature. In contrast to the usually considered percolation transition in the non-uniform medium induced by the localization of charge carriers in the fluctuating electric potential, the studied transition is connected with their localization in the fluctuating magnetic potential produced by magnetized impurities (more accurately – in the combined fluctuating potential). When decreasing temperature, the magnetization of magnetic impurities in the semiconductor becomes higher and even at the invariable (temperature independent) amplitude of the electric potential, the magnetic component of the total potential increases. With increasing fluctuation amplitude, the Fermi level of charge carriers sinks deeper and deeper into the growing tail of density of states until it falls under the percolation level. For that, fluctuations of the total potential have to run up to some critical value. On reaching that value, the transition occurs from the metal conductivity to the activation one (the metal-insulator transition).

Introduction

The role of large-scale fluctuations of the electric potential in traditional (non-magnetic) doped semiconductors is well known [1]. Such a fluctuating potential appears usually in highly-compensated semiconductors where concentrations of charged impurities (donors and acceptors) are high and the concentration of screening mobile charge carriers is low, that results in a large screening length $\ell_s$, defining the spatial scale of electric potential fluctuations. In that case, the average amplitude of the fluctuation potential is also high that leads to the localization of charge carriers and results in the activation character of the system conductivity: it is controlled by the thermal activation of charge carriers from the Fermi level to the percolation level and falls down exponentially with lowering temperature. In the absence of the impurity compensation, the charge carrier concentration is so high that any perturbations of the electrostatic nature are effectively screened, and the spatial scale of the potential coincides with the extent of impurity density fluctuations. The depth of such a short-scale potential relief is relatively shallow and does not lead to the charge carrier localization – the conductivity keeps to be metal one.

In diluted (but nevertheless, highly-doped) magnetic semiconductors (of Ga$_{1-x}$Mn$_x$As type), in addition to above mentioned fluctuations of the electric potential, the new perturbation source appears – specifically, fluctuations of the magnetic potential concerned with fluctuations of the local magnetization in such a semiconductor [2]. That potential is, in fact,

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the potential of the exchange interaction of mobile charge carriers with magnetic impurities \[3\] (for instance, via the RRKKY mechanism) which fluctuates in accordance with fluctuations of the concentration and the local magnetization of those impurities.

Within the wells of the magnetic potential, mobile charge carriers with a certain spin direction are accumulated while the carriers of the opposite spin direction are pushed out. The spatial scale $\ell$ of magnetic fluctuations is now determined not by the electrostatic screening but by the characteristic length of the magnetic interaction of impurities and the correlation length of their arrangement in the semiconductor bulk. However, in diluted magnetic semiconductors, there is usually $\ell \sim \ell_s$ and, thus, spatial scales of the magnetic (exchange) and Qoulomb potentials agree closely.

That means the constructive superposition of both reliefs, and so the average total amplitude of the potential relief becomes to be higher. The medium arises where the concentration and the spin polarization of charge carriers are strongly non-uniform, and the degree of that non-uniformity is substantially defined by the local magnetization of the system.

Increasing magnetization with lowering temperature promotes strengthening the spatial localization of charge carriers and in a number of cases could stimulate the metal-insulator transition \[4\]. Percolative metal conductivity, characteristic for non-uniform systems, changes into the conductivity of the activation type. That occurs when under some external factors (such as temperature, magnetic field, etc.) the Fermi level falls below the percolation level. One of possible mechanisms is as follows. The fluctuating potential leads to appearing the density of states tail into which both the percolation and Fermi levels are pulled. However, rates of those levels’ movement are different, and if they change the relative position the metal-insulator transition occurs. The possibility of such a model is investigated in the present work.

Similar transitions have been repeatedly observed in various systems with magnetic impurities coming into ferromagnetic state at lowering temperature. Thus, for example, in \[5\] the resistivity temperature dependencies of the magnetic semiconductor Cd$_{0.95}$Mn$_{0.05}$Se (in which the electron concentration $n$ being varied by means of the additional doping by In), have been studied. At relatively low electron concentrations ($n \lesssim 10^{18}$ cm$^{-3}$), the resistivity has sharply increased at lowering temperature, that could be interpreted as the transition in the insulator state. The lower $n$, the higher the specific temperature of that transition. Analogous effect has been observed for the compound Ga$_{1-x}$Mn$_x$As with $x \sim 0.02$ \[6\]. Similar process occurs also in Ge, strongly doped (by using ion implantation) with Mn-atoms, whose relative concentration being of 2-4\% \[7\].

We believe that in all those cases the nature of the metal-insulator transition is the same, namely, the localization of charge carriers in the fluctuating magnetic potential which amplitude increases with lowering temperature along with the magnetization of magnetic impurities. Investigating and describing the mechanism of that transition is the object of the present paper.

**Fluctuations of the magnetic potential**

It is convenient to characterize the non-uniform magnetization $M(r)$ of impurities (to be definite, Mn atoms are borne in mind below) by the coordinate dependent local magnetization $j(r) \equiv M(r)/M_s$, where $M_s$ is the saturation magnetization. Non-zero local magnetization ($0 \leq j \leq 1$) of Mn atoms with the spin $S_{Mn} = 5/2$ leads to the non-uniform local spin polarization of holes which is reflected in the fact that the local concentration $p^-(r)$ of holes
with the spin being antiparallel to the local impurity magnetization exceeds the concentration
$p^+(r)$ of holes with the opposite spin orientation. At that, the local degree of the hole
polarization $\xi(r) = [p^-(r) - p^+(r)]/p(r)$ is non-zero ($p(r) = p^-(r) + p^+(r)$ is the total local
hole concentration.) The hole polarization could be interrelated formally with the action of
the effective spin-dependent magnetic potential $U_{mag}$

$$U_{mag}(r) = xN_0a^3J_{pd}\sigma S_{Mn,j}(r),$$

where $N_0 \approx 8 \cdot 10^{21}$ cm$^{-3}$ is the concentration of Ga-sites in the GaAs-lattice, $x$ is the fraction
of those sites being taken by Mn atoms, $a$ is the lattice constant, $\sigma = \pm 1/2$ is the hole spin,
$J_{pd} = 1.2$ eV is the energy of the exchange interaction between mobile holes and localized $d$-electrons of Mn atoms [6]. In accordance to (1), major holes (possessing the preferred spin
orientation) are accumulated in the high magnetization areas, whereas minor ones, conversely,
are ejected in low magnetization areas.

One could found the relation between amplitudes of the magnetic and electrostatic potentials for the impurity concentration fluctuation of the dimension $R_f$ by noticing that the latter could be estimated as $U_{el} \sim (e^2/\kappa R_f)(4\pi xN_0R_f^3)^{1/2} \sim e^2/\kappa R_f$ ($\kappa \sim 10$ is the dielectric susceptibility, $\ell_s \sim a$) $[1]$. Then

$$\frac{U_{mag}}{U_{el}} \sim \frac{jJ_{pd}}{(e^2/\kappa R_f)} \sim \left(\frac{R_f}{a}\right)j,$$

so at $j \sim 1$ we have $U_{mag} \gg U_{el}$ for fluctuations of the dimension $R_f \gg a$. In that case, it
is unacceptable to ignore the magnetic potential. However, more important characteristics of the magnetic relief is the average amplitude $\langle \Delta U_{mag}\rangle$ of the potential fluctuations (cf. below).

Let, in the absence of the magnetization ($j = 0$), the Fermi energy of charge carriers (holes) be $\varepsilon_F$. The magnetic potential (1) originating with appearing magnetization results in the splitting of the hole band into two spin sub-bands with effective Fermi energies (reckoned from edges of those sub-bands) $\varepsilon_F + U_{mag}(r)$ and $\varepsilon_F - U_{mag}(r)$. Two different effective Fermi momenta

$$k_F^\pm(r) = k_F \left(1 \pm \frac{U_{mag}(r)}{\varepsilon_F}\right)^{1/2},$$

correspond to those energies, where $k_F = (2m^*\varepsilon_F/h^2)^{1/2}$, $m^* \approx 0.5m_0$ is the effective hole mass (at $U_{mag}(r)/\varepsilon_F > 1$, $k_F(r) = 0$).

Under the conditions of the uniform magnetization ($j = \text{Const}$) the momenta $k_F^\pm$ are independent of coordinates and, taking into account the spin splitting of the hole band, the expression for the interaction energy $w(\rho)$ of two magnetic atoms, spaced by the distance $\rho$, could be written as

$$w(\rho) = I_0\Phi(\rho),$$

where the range function $\Phi(\rho)$ depends on the mechanism of the indirect interaction of mag-
netic impurities and, by the example of the RKKY interaction, reads [8]

$$\Phi(\rho) = \left(\frac{a}{\rho}\right)^4 \left[\sin \theta^+(\rho) - \theta^+(\rho) \cos \theta^+(\rho) + \sin \theta^-(\rho) - \theta^-(\rho) \cos \theta^-(\rho)\right] \exp(-\rho/\ell),$$

$$I_0 = \frac{1}{(4\pi)^3} \left(\frac{ma^2}{h^2}J_{pd}^2\right), \quad \theta^\pm(\rho) = 2k_F^\pm \rho.$$
The exponential factor in (4) allows for the finite length $\ell$ of the hole spin relaxation \[8\] (being equal to their collision length, in the simplest case).

Notice, with a view of the present work the concrete form of the indirect interaction of magnetic impurities is not a matter of principle. RKKY interaction is used as a model only, permitting to carry later calculations up "to digits".

Generalization of the function (4) for the case of the non-uniform magnetization is made by replacing phases $\theta^\pm(\rho)$ with their average magnitudes

$$
\theta^*_\pm(\rho) = \frac{\sqrt{2} \rho}{\pi} \int_0^\infty k_F(s)ds = 2k_F \int_0^\rho \sqrt{1 \pm A_j(s)}ds,
$$

where $A = xN_0a^3J_{pd}S\mu_a/\varepsilon_F$, and the integration is executed along the line connecting impurities \[8\]. Then the function $\Phi(\rho)$ transforms into the functional of the spatially non-uniform magnetization:

$$
\Phi(\rho) \rightarrow \tilde{F}[A_j(r), \rho] \equiv 
\equiv \left(\frac{a}{\rho}\right)^4 \left[\sin \theta^*_\pm(\rho) - \theta^*_\pm(\rho) \cos \theta^*_\pm(\rho) + \sin \theta^*_\pm(\rho) - \theta^*_\pm(\rho) \cos \theta^*_\pm(\rho)\right]e^{-\rho/\ell}.
$$

At low magnetization $(j \ll 1)$, the magnetic potential (1) is also small and the relation (7) takes the standard form.

As could be seen from Eq. (6), the non-uniformity of the magnetization plays the significant role in that case only when $A_j \sim 1$ (i.e., the magnetic potential is comparable with the Fermi energy). Let us estimate the parameter $A$ for Ga$_{1-x}$Mn$_x$As semiconductor. Due to the compensation, the hole concentration $p$ is always lower than the concentration $xN_0$ of Mn atoms (acceptors) positioned in Ga-sites. Nevertheless, $p/\left(xN_0\right) \gtrsim 0.3$ at $x = 0.05$. The estimation for that case gives $A \sim 1$ \[8\]. Thus, the magnetization non-uniformity should be taken into account in every system area with the local magnetization $j \sim 1$.

Further calculations relate to the simplest case when the magnetization has the same direction anywhere (for instance, due to the strong uniaxial magnetic anisotropy), i.e., $j(r)$ is the scalar value.

The energy $W_{\text{RKKY}}$ of the indirect interaction of a given spin $S_i$ with its surroundings is determined by the sum $W_{\text{RKKY}} = \sum_{j=1}^{\infty} w(\rho_{ij})$. The distance $\rho_{ij}$ could not be smaller that the distance $a_0 = N_0^{-1/3}$ between two neighbor sites of Ga sublattice accessible for magnetic impurities (for the diluted Ga$_{1-x}$Mn$_x$As semiconductor $a_0 = a/\sqrt{2}$, where $a \approx 5\text{\AA}$ being the lattice constant). In the continual approximation the sum could be replaced by the integral

$$
W_{\text{RKKY}}(r) = I_0N_0 \int \tilde{F}[A_j(r'), |r - r'|] x(r')j(r')d^3r',
$$

where the integration executed over the volume occupied by impurities.

To obtain qualitative results, below we will not go beyond the simple model range function $\Phi(\rho)$, depending on the distance between impurity atoms only and coinciding with that for the uniform system. Then, in spherical coordinates, where a given impurity atom is situated at the distance $h$ from the coordinate origin,

$$
W(h) = I_0N_0 \int \int \Phi[\rho(h, \varphi, \theta)]x(r, \varphi, \theta)j(r, \varphi, \theta)r^2 \sin \theta drd\varphi d\theta,
$$
where $\rho(h, r, \varphi, \theta) = (r^2 + h^2 - 2rh \sin \theta \cos \varphi)^{1/2}$.

Hereinafter, we take an interest in spatial dependencies of the impurity concentration $x(r)$ and magnetization $j(r)$ only. Taking into account the angle dependencies of those values could not lead to the principal variation of physical parameters of the length dimension, such as "screening length" of the point magnetic perturbation (delta-like burst of the magnetic impurity concentration). Therefore, in Eq. (9) we keep the spatial dependence of above mentioned parameters only (or, in other words, replace them by values, averaged over angles). Then Eq. (9) takes the form

$$W(h) = I_0 N_0 \int_r \int_\varphi \int_\theta \Phi[\rho(h, r, \varphi, \theta)] x(r) j(r) r^2 \sin \theta dr d\varphi d\theta, \quad (10)$$

where the integration range is defined by the condition $\rho(h, r, \varphi, \theta) \geq a_{\text{min}}$. For the function $\Phi(\rho)$ which is non-divergent at $\rho \to 0$, integrating could be performed over the whole space, and the convergence of the integral (10) is guaranteed by the fast decay of the range function.

In the latter case, the self-consistent equation

$$j(h) = B_S \left[ \frac{\tau}{1/a_0^2} \int_{r=0}^\infty K(h, r) x(r) j(r) r^2 dr \right], \quad (11)$$

where

$$K(h, r) = \int_\varphi \int_\theta h(\rho/a_0) \Phi[\rho(h, r, \varphi, \theta)] \sin \theta d\varphi d\theta, \quad (12)$$

$\tau = kT/I_0$ is the reduced temperature, $h(t)$ is the unit Heaviside function. That is the integral equation defining the spatial dependence of the local magnetization $j(r)$ at a given spatial distribution $x(r)$ of the magnetic impurity concentration. For the uniform doping, when $x(r) = x_0$, the system magnetization is also uniform: $j(r) = j_0$.

For the average impurity concentration $x_0$, the number of impurity atoms in the volume $V$ is, in average, $\bar{N} = x_0 N_0 V$ with the standard deviation $\bar{N}^{1/2}$ from that value. The relevant fluctuation of the relative concentration equals $\Delta x = \pm \sqrt{x_0 (a_0^3/V)}$, or

$$\Delta x = \pm (a_0/R_f)^{3/2} \sqrt{(3/4\pi)x_0} \quad (13)$$

for the spherical fluctuation of the radius $R_f$.

Let us consider the magnetic perturbation in the uniform semiconductor as the Gauss spherically symmetrical fluctuation of the magnetic impurity concentration in the coordinate origin: $x(r) = x_0 + \delta x(r)$, where $\delta(x) = \Delta x \exp(-r^2/R_s^2)$. The "response" of the system to that perturbation appears as the non-uniformity of its magnetization $j(r)$ about a point of that fluctuation. The size of the relevant non-uniform area and the magnitude of the magnetization deviation from the bulk value $j_0$ could be found with the help of Eq. (11).

That phenomenon is the magnetic analog of screening electric charges in strongly doped semiconductors with impurity fluctuations. In this case, the average amplitude and the spatial scale of the fluctuating electric potential is determined by optimal impurity fluctuations with the size close to the screening length [1]. The same characteristics of the fluctuating magnetic
potential are defined by the characteristic length of the magnetic impurity interaction (cf. Eqs. (3), (4)) and to a large extent, by temperature, as well (cf. Eq. (11)).

Fig. 1 demonstrates spatial perturbations $U_{\text{mag}}(h)$ of the magnetic potential, generating by spherical fluctuations of the impurity concentration (situated in the coordinate origin) whose amplitude and size are interrelated by Eq. (13). They are calculated in the course of the numerical solution of the equation (11) by successive approximations’ method (for some realistic set of parameters $x_0$, $k_Fa^3$, $\ell/a$). At the large distance from the origin, the magnetic potential tends to its bulk value characteristic for the uniform medium with the impurity concentration $x_0$. The most deviation from that value is observed, naturally, near the origin where the center of the impurity fluctuation is located. The variation of the magnetic potential

$$\Delta U_{\text{mag}} = U_{\text{mag}}(h = 0, \Delta x > 0) - U_{\text{mag}}(h = 0, \Delta x < 0),$$

defined as the difference between magnetic potentials in centers of the positive ($\Delta x > 0$) and negative ($\Delta x < 0$) fluctuations, depends, naturally, on the amplitude $\Delta x$ (or on the size $R_f$, cf. Eq. (13)) of the fluctuation. It is hereinafter important that the average amplitude of the magnetic potential fluctuations coincides with $\Delta U_{\text{mag}}$ on the order of value and defined by the characteristic spatial scale of impurity concentration fluctuations.

In [9] that scale is identified with the correlation length of impurity arrangement which (taking into account the mutual attraction of Mn atoms in GaAs) is estimated as $R_f \approx (3 - 5)a_0$. Basing upon that estimate, we accept the typical fluctuations being of the radius $R_f = 5a_0$. At the average impurity concentration $x_0 = 0.05$, that results in the concentration fluctuation equal to $\Delta x \approx 0.03$ (cf. Eq. (13)). For those fluctuations, according to Fig. 1 $\Delta U_{\text{mag}} \approx 0.03J_{pd} \approx 30 \text{ meV}$. It is just the average amplitude of magnetic potential fluctuations (its difference between maximum and minimum) in the considered diluted magnetic semiconductor. Its temperature dependence is shown in Fig. 2 – magnetic fluctuations arise with appearing non-zero magnetization and with further temperature lowering their amplitude is saturated in compliance with the magnetization saturation.

The relation between amplitudes of the magnetic and electrostatic potentials for the fluctuation of impurity density of the radius $R_f$ could be found, noticing that the latter could be estimated as $\gamma_e \sim (e^2/\kappa R_f)(\Delta x N_0 R_f^3)$ [1]. Herefrom, it follows

$$\frac{\Delta U_{\text{mag}}}{\gamma_e} \sim \left( \frac{R_f}{a} \right) j,$$

so that $\Delta U_{\text{mag}} \gtrsim \gamma_e$ at $j \sim 1$.

**Metal-insulator transition**

If the magnetization is low ($j \ll 1$), the magnetic potential and spin polarization of charge carriers (holes) could be neglected. In that case, their transport is defined by the possibility of Anderson localization in the random electrostatic potential and could be of the metal or thermoactivation (insulator) type depending on the mutual disposition of the Fermi level $\varepsilon_F$ and the percolation one $U_p$. The latter is determined by the condition $\int_{-\infty}^{U_p} F(U) dU = \theta_p$, where $F(U)$ is the distribution function of random potential, $\theta_p \approx 0.17$ is the fraction of the space where the potential $U < U_p$ [1]. For the Gauss function $F(U) = (2\pi\gamma_e^2)^{-1/2} \exp(-U^2/2\gamma_e^2)$ (symmetrical relative to the level $U = 0$, corresponding to the edge of the mobile charge carriers’ band) we have $U_p \approx -0.95\gamma_e$. 

6
In the diluted magnetic semiconductor, which is a slightly-compensated doped semiconductor, the amplitude of the electrostatic potential is relatively small and the charge carrier concentration is so high that the Fermi level is positioned above the percolation level. That results in the metal conductivity.

Engaging the magnetic fluctuation potential at low temperatures changes the potential relief significantly. Since at low temperatures current carriers are strongly polarized (those ones prevail, whose spin is antiparallel to spins of polarized magnetic impurities), it is sufficient to take into account the magnetic potential for such carriers only (that means $\sigma = -1/2$ in (1)). Exactly such a simple model is applied below. Statistic properties of the total potential, which is the sum of the electrostatic and mentioned magnetic potentials, are described by the distribution function, whose halfwidth enlarges (comparing to the initial distribution function of the electric potential) approximately by the magnitude $\gamma_m = \Delta U_{mag}/2$:

$$F(U) = \frac{1}{\sqrt{2\pi(\gamma_e + \gamma_m)}} \exp \left[ -\frac{1}{2} \left( \frac{U}{\gamma_e + \gamma_m} \right)^2 \right].$$  \hspace{1cm} (15)

Then, with increasing the magnetic potential $\Delta U_{mag}$, the percolation level (defined by the former condition $\theta_p = 0$) drifts downward according to the simple linear low

$$U_p \approx -0.95\gamma, \gamma = \gamma_e + \gamma_m.$$  \hspace{1cm} (16)

The position of the Fermi level depends also on the total amplitude $\gamma$ of the fluctuation potential: appearing tail of the density of states ”pulls” it down. Unlike the density of states $g_0(\varepsilon) = (2m^*)^{3/2}\sqrt{\varepsilon}/2\pi^2\hbar^3$ in the uniform medium, turning into zero at $\varepsilon \leq 0$ ($\varepsilon = 0$ corresponds to the edge of the charge carrier band), the tailed density of states $g(\varepsilon)$ in a medium with fluctuating impurity concentration is determined by the relation [1]

$$g(\varepsilon) = \frac{(2m^*)^{3/2}\sqrt{\gamma}}{2\pi^2\hbar^3} G_0(\varepsilon/\gamma),$$  \hspace{1cm} (17)

where

$$G_0(X) = \frac{1}{\sqrt{\pi}} \int_{-\infty}^{X} e^{-y^2} (X - y)^{1/2} dy.$$  \hspace{1cm} (18)

At the invariable concentration $n$ of degenerate charge carriers, the Fermi level $\mu$ shifted due to the fluctuations (of the average amplitude $\gamma$) could be found from the relationship

$$n = \int_{0}^{\mu_0} g_0(\varepsilon) d\varepsilon = \int_{-\infty}^{\mu} g(\varepsilon) d\varepsilon$$

($\mu_0$ is the Fermi energy in the uniform medium), which leads to the equation

$$\frac{1}{\sqrt{\pi}} \int_{-\infty}^{X} \left[ \int_{-\infty}^{X} e^{-y^2} (X - y)^{1/2} dy \right] dX = \frac{2}{3} \left( \frac{\mu_0}{\gamma} \right)^{3/2}.$$  \hspace{1cm} (19)

The result of solving Eq. (19) is represented in Fig. 3. At a small fluctuation amplitude, the Fermi energy coincides practically with that for the uniform medium ($\mu \approx \mu_0$). However,
with increasing amplitude $\gamma$ it drifts quickly down into the range of developing tail of density of states.

If drifting the Fermi level $\mu$ can result in changing the character of the conductivity (metal or activation) depends on how the percolation level $U_p$ shifts (cf. (16)). Fig. 4 shows the arrangement of those two levels as a function of the total fluctuation amplitude $\gamma$. Evidently, at $\gamma \approx 10\mu_0$ their mutual disposition changes: at small $\gamma$ values, the Fermi energy level is above the percolation level and at large $\gamma$, it lies lower. That means the transition from the metal conductivity to the activation one.

Such a transition could happen under the action of different factors. One could influence either electrostatic component $\gamma_e$ of the total fluctuation amplitude $\gamma$, or the magnetic component $\gamma_m$. For example, the well-known metal-insulator transition observing under varying the compensation degree in strongly doped compensated semiconductors [1] relates to the first case.

The second case corresponds to the above considered temperature transition in magnetic semiconductors associated with the dependence of the component $\gamma_m$ on the local magnetization varying with temperature (cf. (14)). Qualitative notion concerning the temperature dependence of the resistivity $\rho(T)$ of the magnetic semiconductor could be obtained with using the simple model relation

$$
\rho(T) = \begin{cases} 
\rho_0 & U_p < \mu \\
\rho_0 \exp[(U_p - \mu)/kT] & U_p > \mu 
\end{cases},
$$

(20)

if one specifies the average amplitude $\gamma_e$ of "seed" electrostatic fluctuations.

Dependencies $\rho(T)$, found with the described procedure, are presented in Fig. 5. They demonstrate the metal-insulator transition induced by the magnetic potential fluctuations at lowering temperature, and look qualitatively like experimental dependencies $\rho(T)$ for considered systems (see the insert in Fig. 5; slow temperature upgrowth of Ge$_{0.98}$Mn$_{0.02}$ resistivity in the metal state is connected with carrier scattering by phonons). The characteristic temperature of such a transition depends significantly on the fluctuation amplitude $\gamma_e$ of the initial electrostatic potential: the higher $\gamma_e$, the lower that temperature. Since $\gamma_e \propto x_0^{1/2}$ (cf (13)), the transition temperature should decrease with increasing the impurity concentration $x_0$ that also agrees with experiments [3, 6, 7].

Conclusions

In conclusion, we have considered the metal-insulator transition happening with lowering temperature in semiconductors with magnetic impurities. Unlike the percolation transition in the non-uniform medium induced by the charge carriers localization in the fluctuating electric potential of charged impurities [1] (of the average amplitude $\gamma_e$), the considered transition is connected with the localization in the fluctuating magnetic potential (of the average amplitude $\gamma_m$) generated by the impurity magnetization, or more accurately – in the total fluctuation potential (of the average amplitude $\gamma = \gamma_e + \gamma_m$). Since with lowering temperature the magnetization of magnetic impurities in the semiconductor increases, even under the invariable (temperature independent) electric potential amplitude $\gamma_e$ the magnetic component $\gamma_m$ of the total potential enlarges. The metal-insulator transition occurs when potential fluctuations becomes so high that the Fermi level $\mu$ falls into the range of localized states below the percolation level $U_p$. 
The transition temperature is defined by establishing the condition $\mu(T) \leq U_p(T)$, where, according to (16), $U_p(T) = 0.95 \gamma(T)$, and $\mu$ is determined by the equation (19). Its solution could be written in the form $\mu(T) = F[\gamma(T)]$, where $F(\gamma)$ is some function whose plot (for a certain set of parameters) is represented in Fig. 4. Thus, the transition temperature $T_c$ is found from the condition $F[\gamma(T)] < 0.95 \gamma(T)$, or $\gamma(T) > \gamma_c$, where $\gamma_c$ is some critical magnitude of the average amplitude of total potential fluctuations. The reason for the transition consists in that with increasing fluctuation amplitude the Fermi level sinks deeper and deeper into the growing tail of the density of states until (at the beginning of the condition $\gamma > \gamma_c$) it falls below the percolation level. At that, the transition from the metal conductivity to the thermoactivation one happens (the metal-insulator transition).

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Figure captions

Fig. 1. Spatial perturbations $U_{\text{mag}}(h)$ of the magnetic potential generated by spherical fluctuations of the impurity concentration (situated in the coordinate origin). Upper curves are for "positive" fluctuations ($\delta x > 0$), lower ones – for "negative" fluctuations ($\delta x < 0$). Accepted parameters: $x_0 = 0.05$, $\tau = 0.05$, $k_F a = 0.1$, $\ell = 5a$.

Fig. 2. Temperature dependence of the average amplitude $\Delta U_{\text{mag}}$ for magnetic potential fluctuations connected with spherical impurity density fluctuations of the radius $R_f = 5a_0$. Accepted parameters: $x_0 = 0.05$, $\tau = 0.05$, $k_F a = 0.1$, $\ell = 5a$.

Fig. 3. Shifting the Fermi energy $\mu$ as a function of the total potential fluctuation amplitude $\gamma$. Dashed line is the unshifted Fermi energy $\mu_0$ (in the absence of fluctuations).

Fig. 4. Mutual arrangement of the Fermi level $\mu$ and the percolation level $U_p$ as a function of the total potential fluctuation amplitude $\gamma$. Dashed line separates areas of the metal and activation ($I$) conductivities.

Fig. 5. Model temperature dependencies of the magnetic semiconductor resistivity $\rho(T)$ for two magnitudes of the electric potential fluctuation amplitude $\gamma_e$. Accepted parameters: $x_0 = 0.05$, $k_F a = 0.1$, $\ell = 5a$, $J_{pd} = 1.2$ eV, $\mu_0 = 5$ meV. In the insert: experimental temperature dependencies of the resistivity for Ga$_{0.985}$Mn$_{0.015}$As [6] and Ge$_{0.98}$Mn$_{0.02}$ [7].
\[ x(h) j(h) = U_{\text{mag}}(h) / (J_{pd} \sigma S) \]
\[ \Delta U_{\text{mag}} / (J_{pd} \sigma S) \]
$U_p / \mu_0 = -0.95 \gamma / \mu_0$

percolation level $U_p$

Fermi level $\mu$

$\mu / \mu_0$

$\gamma / \mu_0$
\[ \rho/\rho_0 \]

\[ \rho, \Omega \cdot \text{cm} \]

\[ T, K \]

\[ \gamma_e = 40 \text{ meV} \]

\[ 0, 0.02, 0.04, 0.06, 0.08 \]

\[ 0, 50, 100, 150, 200 \]

Ga\textsubscript{0.985}Mn\textsubscript{0.015}As
F. Matsukura, e.a. [6]

Ge\textsubscript{0.98} : Mn\textsubscript{0.02}
O. Riss, e.a. [7]