Heavy ions at the LHC: Selected predictions

Yacine Mehtar-Tani* and Georg Wolschin
Institut für Theoretische Physik der Universität, Philosophenweg 16, D-69120 Heidelberg, Germany
*Now at Departamento de Física de Partículas and IGFAE, Universidade de Santiago de Compostela, Spain
E-mail: wolschin@uni-hd.de

Abstract. Baryon transport in relativistic heavy-ion collisions is investigated within a gluon saturation model. The theoretical results are compared with Pb + Pb data at SPS, and Au + Au data at RHIC energies. Predictions are made for net-baryon and net-proton rapidity distributions in central Pb + Pb collisions at CERN LHC energies of up to \( \sqrt{s_{NN}} = 5.5 \) TeV both at forward rapidities, and in the central rapidity region where data will soon be available.

1. Introduction
With the CERN Large Hadron Collider LHC now in operation for proton-proton collisions at center-of-mass energies of up to 7 TeV [1, 2], the advent of heavy-ion collisions at the LHC is expected in November 2010, and corresponding theoretical predictions will then be tested. In this note such predictions for several selected observables will be presented.

We calculate rapidity distributions of net baryons, and net protons (\( p - \bar{p} \)) in central heavy-ion collisions using an approach that is based on quantum chromodynamics and in particular, on the gluon saturation model [3, 4, 5, 6]. Our specific model for net baryons is described in detail in [7, 8, 9]. A complementary phenomenological nonequilibrium-statistical model that is not based on QCD had been formulated earlier [10] to predict the corresponding observables at LHC energies — and also charged-hadron pseudorapidity distributions — with similar results for net baryons.

The calculations for net-baryon rapidity distributions within our QCD-based model are reviewed in Sec. 2, and results at LHC energies are given in Sec. 3. In Sec. 4 the analysis is concentrated on the midrapidity region where data will soon be available. Conclusions are drawn in Sec. 5.

2. Rapidity distributions for net baryons based on QCD
Gluon saturation has been the focal point of important and interesting particle-physics investigations since many years. Its observation would provide access to a new regime of quantum chromodynamics where high-density gluons form a coherent state. In regions of large parton densities the physics is governed by a single hard scale \( Q_s \gg \Lambda_{QCD} \) which increases with energy and thus allows the use of small-coupling techniques [3, 4, 5, 6]. In this regime gluon recombination starts to compete with the exponentially increasing gluon splitting, and the gluon distribution function is expected to saturate.
At the HERA, some evidence for gluon saturation in the proton had been found in deep inelastic $e+p$ collisions at high energy and low values of Bjorken-$x$, but the results are still open to interpretation [11]. The existence of geometric scaling as predicted by the color glass theory as an approach to saturation physics had indeed been confirmed, constituting the most important evidence for saturation so far [12].

Since the saturation scale is enhanced by a factor $A^{1/3}$ in heavy ions as compared to protons, it is natural to investigate saturation in relativistic heavy-ion collisions, as has been done by many authors [13]. Most theoretical investigations concentrate on charged-hadron production from inclusive gluon interactions, and in the central rapidity region a reasonable understanding has been achieved in the color glass condensate framework [6, 14, 15, 16] through inclusive gluon production [17, 18]. However, the valence-quark scattering off the gluon condensate as an observable in net-baryon distributions [7, 8] is expected to provide interesting new information on gluon saturation, and on geometric scaling [12].

Here the most promising effects arise at very forward angles, or correspondingly large values of the rapidity $y \approx 5 - 8$ at LHC energies of $\sqrt{s_{NN}} = 5.5$ TeV for Pb + Pb, with a beam rapidity of 8.68. For symmetric systems, two symmetric fragmentation peaks are expected to be present in the net-baryon distributions at forward/backward rapidities, as was shown in the RDM-calculations in the previous section. In particular, we have discussed in [7] that it is in principle possible to determine the growth of the saturation-scale, $\lambda \equiv d \ln Q_s/dy_b$ from the position of the fragmentation peak in rapidity space. Here the beam rapidity is $y_b = 1/2 \cdot \ln[(E + p_L)/(E - p_L)] \approx -\ln \sqrt{s}/m$ at beam energy $E$ and longitudinal momentum $p_L$ with the nucleon mass $m$.

In the region of large values of Bjorken-$x$ the valence-quark parton distribution in the projectile is well-known, and can hence be used to access the gluon distribution at small $x$ in the other nucleus where saturation is expected to occur due to the competition of gluon recombination with the exponentially increasing gluon splitting [14, 15, 19, 20, 16].

For the next years of LHC operation, however, experimental investigations of central heavy-ion collisions with particle identification will concentrate on the midrapidity region $y \leq 2$ and hence, we focus our predictions for net-baryon distributions at LHC energies to this region. It turns out that here the saturation-scale exponent $\lambda$ can not be determined from net-baryon distributions because the dependence of the distribution function on $\lambda$ is too weak near midrapidity.

The differential cross section for valence quark production in a high-energy nucleus-nucleus collision is calculated from [21, 22, 23]

$$\frac{dN}{d^2p_Tdy} = \frac{1}{(2\pi)^2} \frac{1}{p_T^2} x_1q_v(x_1,Q_f) \varphi(x_2,p_T),$$

where $p_T$ is the transverse momentum of the produced quark, and $y$ its rapidity. The longitudinal momentum fractions carried, respectively, by the valence quark in the projectile and the soft gluon in the target are $x_1 = p_T/\sqrt{s}\exp(y)$ and $x_2 = p_T/\sqrt{s}\exp(-y)$. The factorization scale is usually set equal to the transverse momentum, $Q_f \equiv p_T$. We have discussed the gluon distribution $\varphi(x,p_T)$ and details of the overall model in [7].

The contribution of valence quarks in the other beam nucleus is added incoherently by changing $y \rightarrow -y$. The valence quark distribution of a nucleus, $q_v \equiv q - \bar{q}$, is given by the sum of valence quark distributions $q_{v,N}$ of individual nucleons, $q_v \equiv Aq_{v,N}$, where $A$ is the atomic mass number.

Assuming that the rapidity distribution for net baryons is proportional to the valence-quark rapidity distribution up to a constant factor $C$, one obtains by integrating over $p_T$,

$$\frac{dN}{dy} = \frac{C}{(2\pi)^2} \int \frac{d^2p_T}{p_T^2} x_1q_v(x_1,Q_f) \varphi(x_2,p_T).$$ 

(2)
It turns out that this is indeed a good approximation at sufficiently high energy, in particular, when comparing to Au + Au data from RHIC, and it is expected to be valid at LHC as well [7, 8].

One important prediction of the color glass condensate theory is geometric scaling: the gluon distribution depends on $x$ and $p_T^2$ only through the scaling variable $p_T^2/Q_s^2(x)$, where $Q_s^2(x) = A^{1/3}Q_0^2 x^{-\lambda}$, $A$ is the mass number and $Q_0$ sets the dimension. This has been confirmed experimentally at HERA [12]. The fit value $\lambda = 0.2 - 0.3$ agrees with theoretical estimates based on next-to-leading order Balitskii-Fadin-Kuraev-Lipatov (BFKL) results [24, 25]. To show that the net-baryon distribution reflects the geometric scaling of the gluon distribution, the following change of variables has been proposed in [7]: $x_1 \equiv x$, $x_2 \equiv x e^{-2y}$, $p_T^2 \equiv x^2 s e^{-2y}$. Thus, Eq. (2) for the rapidity distribution can be rewritten as

$$\frac{dN}{dy}(\tau) = \frac{C}{2\pi} \int_0^1 \frac{dx}{x} x q_v(x) \varphi(x^{2+\lambda} e^\tau),$$

where $\tau = \ln(s/Q_0^2) - \ln A^{1/3} - 2(1 + \lambda)y$ is the corresponding scaling variable. Hence, the net-baryon multiplicity in the peak region is only a function of a single scaling variable $\tau$, which relates the energy dependence to the rapidity and mass number dependence. In the fragmentation region, the valence quark distribution is only very weakly dependent on $Q_f$. 

**Figure 1.** Rapidity distribution of net baryons in central (0 – 5%) Pb + Pb collisions at SPS energies of $\sqrt{\text{s}_{NN}} = 17.3$ GeV (left frame). The theoretical calculation for $\lambda = 0.2$ and $Q_0^2 = 0.04$ GeV$^2$ is compared with NA49 results that have been extrapolated from the net-proton data (open circles [26]). Black diamonds are more recent preliminary NA49 data points [27]. At RHIC energies of $\sqrt{\text{s}_{NN}} = 62.4$ GeV (middle frame, 0 – 10%) and 200 GeV (right frame, 0 – 5%) for central Au + Au, our corresponding theoretical results are compared with BRAHMS net baryon data (circles) [28, 29]. At 200 GeV, triangles are preliminary scaled BRAHMS net proton data points for 0 – 10% [30]. The full lines correspond to the no-fragmentation hypothesis with $Q_0^2 = 0.04$ GeV$^2$ and the dashed lines include fragmentation with $Q_0^2 = 0.1$ GeV$^2$. Arrows indicate the beam rapidities. From Mehtar-Tani and Wolschin [8].

Our results for net-baryon rapidity distributions in central Pb + Pb and Au + Au collisions are shown in Fig. 1. See Mehtar-Tani and Wolschin [8] for a detailed discussion. We compare with SPS NA49 Pb + Pb results at $\sqrt{\text{s}_{NN}} = 17.2$ GeV [26], and BRAHMS Au + Au data at 62.4 GeV and 200 GeV [28, 29, 30, 31]. The estimated numbers of participant are 390, 315 and 357 for $\sqrt{s} = 17.3$, 62.4 and 200 GeV respectively [29, 31].
3. Predictions at LHC energies
A prediction for central Pb + Pb at the maximum LHC energy of 5.52 TeV is shown in Fig. 2 for \( \lambda = 0, 0.15, \) and 0.3. At LHC energies the mid-rapidity region is almost baryon free, we obtain \( dN/dy(y = 0) \sim 4 \) for net baryons at 5.52 TeV. The position of the fragmentation peak is very sensitive to the value of \( \lambda \), with a difference of about 1.5 units of rapidity between the \( \lambda = 0 \) and 0.3 cases. It is possible that the full scaling regime with \( \lambda \) approaching 0.3 can be reached at or beyond LHC energies, but presently none of the LHC-experiments is capable of measuring identified protons or neutrons from central Pb + Pb collisions in the region of the fragmentation peaks. This would be a relevant proposal for future extensions of the detector capabilities at LHC.

With increasing energy (such as from RHIC to LHC) the peaks move apart, the solutions behave like travelling waves in rapidity space, which can be probed experimentally at distinct values of the beam energy, or the corresponding beam rapidity. The peak position as a function of the beam rapidity is \( y_{\text{peak}} = vy_{b} + \text{const} \) with the peak velocity \( v = 1/(1 + \lambda) \). The position of the peak in rapidity space as a function of the beam energy can in principle be determined experimentally, or at least estimated (RHIC). Theoretically, its evolution with energy provides a measure of the saturation scale exponent \( \lambda \). Hence, a precise determination of the net-baryon fragmentation peak position as a function of beam energy would provide detailed information about the gluon saturation scale.

The mean rapidity loss \( \langle \delta y \rangle = y_{b} - \langle y \rangle \) is also shown in Fig. 2, our result is in agreement with the experimental values of baryon stopping that have been obtained at AGS and SPS energies [32, 26]. Assuming that the mean rapidity evolves similarly to the peak position, \( \langle y \rangle \equiv y_{\text{peak}} + \text{const} \), the mean rapidity loss increases linearly at large \( y_{b} \), \( \langle \delta y \rangle = \frac{\lambda}{1 + \lambda} y_{b} + \text{const} \): the slope is related to \( \lambda \).

Hence, the mean rapidity loss that accompanies the energy loss in the course of the slow-down of baryons also provides a potential measure for \( \lambda \) and thus, a test of saturation physics. The grey band in Fig. 2(b) reflects the uncertainty of how to place the remaining baryons that are missing in the present model.

Our result for the mean rapidity loss as function of beam rapidity, or center-of-mass energy, emphasizes the importance of a detailed measurement at LHC energies to allow more definite conclusions about the value of \( \lambda \) from net-baryon distributions in relativistic heavy-ion physics.

4. Net baryons in the midrapidity region
Since net-baryon data in central heavy-ion collisions at large rapidities will not be available for the next years, one first has to concentrate on the midrapidity region. This chapter refers to corresponding predictions [9]. The LHC physics program starts with a center-of-mass proton-proton energy of 7 TeV, the corresponding energy for Pb + Pb (scaling with Z/A) is \( \sqrt{s_{NN}} = 2.76 \) TeV. Predictions for the highest attainable Pb + Pb energy of 5.52 TeV are also shown. Since experimental results will be available for net protons, we calculate these at the highest LHC energy in the midrapidity valley \( |y| < 2 \) instead of net baryons.

In the midrapidity valley Eq. (2) becomes [9]

\[
\frac{1}{A} \frac{dN}{dy} \propto \left( \frac{A^{1/6}Q_{0}}{\sqrt{s}} \right)^{\Delta/(1+\frac{1}{2})} \cosh \left[ 2\Delta \frac{1 + \lambda y}{2 + \lambda y} \right] \quad (4)
\]

which reduces to Eq. (80) in [33] for the special case \( \lambda = 0 \). Here, \( \Delta = 1 - \sqrt{\frac{2\alpha_s C_F}{\pi(1-\lambda)}} \) with \( C_F = (N_C^2 - 1)/2N_C, N_C = 3 \). The value of \( \Delta \) had been fitted to the old preliminary BRAHMS data in [33] , with \( \Delta \simeq 0.47 \), leading to a strong-coupling constant \( \alpha_s \simeq 0.3 \).
Figure 2. Central collisions of Pb + Pb and Au + Au. (a) Rapidity distribution of net baryons in central Pb + Pb collisions at LHC energies of $\sqrt{s_{NN}} = 5.52$ TeV. Theoretical distributions are shown over the full rapidity range including the fragmentation peaks for $\lambda = 0$ (dashed), $\lambda = 0.15$ (solid), and $\lambda = 0.3$ (dotted curve). (b) The mean rapidity loss $\langle \delta y \rangle$ as obtained from our theoretical results is plotted as a function of beam rapidity $y_b$. The star at $y_{beam} = 8.68$ is our prediction for central Pb + Pb at LHC-energies of $\sqrt{s_{NN}} = 5.52$ TeV with $\lambda = 0.2$ and $Q_0^2 = 0.04$ GeV$^2$. Analysis results from AGS Au + Au data (E917, E802/E866, triangles) [32], SPS Pb + Pb data (NA49, square) [26], RHIC Au + Au data (BRAHMS, dots, with triangles as lower and upper limits) [28, 29] are compared with the calculations. From Mehtar-Tani and Wolschin [7, 8].

We now use the analytical form for $dN/dy = a \cosh(by)$ (cf. Eq. (4)) in a direct comparison with BRAHMS net-proton data in central Au + Au collisions at RHIC energies of $\sqrt{s_{NN}} = 0.2$ TeV [28] through a $\chi^2$-minimization of the two parameters $a$ and $b$, where $b = 2\Delta(1+\lambda)/(2+\lambda)$.

Figure 4. Calculated rapidity distributions of net protons in 0%–5% central Pb + Pb collisions at LHC energies of $\sqrt{s_{NN}} = 2.76, 3.94, 5.52$ TeV. Our result for central Au + Au collisions at RHIC energies of 0.2 TeV is compared with BRAHMS data [28] in a $\chi^2$-minimization as in Fig. 1. From Mehtar-Tani and Wolschin [9].

Our comparison with the BRAHMS Au + Au data in the midrapidity region is shown in Fig. 4 for net protons. We display the energy dependence of our net-proton central Pb + Pb results near midrapidity for $\sqrt{s_{NN}} = 2.76, 3.94$, and 5.52 TeV. At $y = 0$ the corresponding values of $dN/dy$ are 1.9, 1.7, and 1.4.

A description for the net-proton rapidity distribution within the relativistic diffusion model (which is not based on QCD, but on nonequilibrium-statistical physics) had been developed in [10]. There the predicted midrapidity value for central Pb + Pb at the LHC energy of $\sqrt{s_{NN}} = 5.52$ TeV is.
5.52 TeV is $dN/dy \simeq 1 – 2.5$ depending on the model parameters and hence, comparable to the present QCD-based result.

5. Conclusion
To conclude, predictions for net-baryon (proton) distributions in central Pb + Pb collisions at LHC energies have been presented. The investigation uses a microscopic approach based on quantum chromodynamics. This transparent QCD-based model \[7, 8\] with well-established parton distribution functions in the context of saturation physics allows to calculate transverse momentum \[8\] and rapidity distributions for net baryons, and also net kaons \[7, 8, 9\].

The underlying physical process is the scattering of valence quarks off the gluon condensate in the respective other nucleus. In the forward rapidity region the position of the fragmentation peak is very sensitive to the gluon saturation scale, such that the saturation-scale exponent could in principle be determined from LHC data should these become accessible in the coming years. In the near future, net-baryon (proton) data in central Pb + Pb collisions at LHC energies will, however, only be available near midrapidity $|y| < 2$. In this region detailed results have been presented, which will soon be compared to LHC heavy-ion data.

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