Manipulation of Colloids by Nonequilibrium Depletion Force in Temperature Gradient

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The non-equilibrium distribution of colloids in a polymer solution under a temperature gradient is studied experimentally. A slight increase of local temperature by a focused laser drives the colloids towards the hot region, resulting in the trapping of the colloids irrespective of their own thermophoretic properties. An amplification of the trapped colloid density with the polymer concentration is measured, and is quantitatively explained by hydrodynamic theory. The origin of the attraction is a migration of colloids driven by a non-uniform polymer distribution sustained by the polymer’s thermophoresis. These results show how to control thermophoretic properties of colloids.

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Introduction.——Gradients of thermodynamic variables such as temperature, chemical potential, and osmotic pressure cause migration of molecules and small particles in fluids[1]. For example in biological cell, coupling of two gradients is often used to promote molecular transport against one of the gradients as in chemiosmosis[2]. In physics and chemistry, novel methods to utilize phoretic properties (electro-, thermo-, and diffusiophoresis) are proposed for transporting and screening particles in laboratory-chip[3, 4] or designing active materials[5]. In thermophoresis, the speed and direction of migration along a temperature gradient are characterized by Soret coefficient, which is generally material-dependent[6, 7, 8, 9, 10]. Diffusiophoresis is a similar phenomenon where colloids move along a gradient of solute molecules[11, 12, 13]. The benefits of them have been used for efficient and amplified transport in microfluidics[14, 15, 16]. However, strong material dependence of Soret coefficients, and difficulty in keeping a stationary solute gradient of diffusiophoresis prevent further development of application of nonequilibrium force by the phoretic effects. Understanding physical mechanism of thermophoresis has made marked progress recently[17, 18, 19], however, it is still challenging to control magnitude of the force to overcome these problems.

In this paper, we demonstrate that a suitable coupling of thermophoresis for polymer solute molecules and diffusiophoresis for a target particle (colloid) largely resolve the problems. More specifically, we report experimental and theoretical studies on a phoretic motion of colloidal particles in a polymer solution under a temperature gradient. We find that a Soret coefficient of a colloid is sensitive to the polymer (PEG) concentration; as increasing the amount of polymer, the Soret coefficient reverses its sign and its magnitude outweighs by far its intrinsic value at the highest polymer concentration studied. The dependence of the Soret coefficient on the polymer is experimentally determined and is corroborated by our hydrodynamic calculations. This novel effect allows us to transport and trap colloids at any desired position by suitably controlling a temperature distribution and the polymer concentration.

Experiment.——In a thin chamber containing a solution, a steep temperature gradient up to 1 [K/µm] was created while keeping the local temperature rise quite small (∆T ∼ 4K) by focusing an infrared laser (Nd:YAG, 1064 nm, power ∼4mW before an objective lens) on a light absorbing metal coated surface of the thin glass chamber (Setup I) as shown in Fig.1a[20]. Using this setup, we measured the distributions of polystyrene beads. Figure 1b shows fluorescence intensity of 100 nm diameter beads (F8803; Invitrogen) in a water solution. The fluorescence intensity became lower at the hot region around laser focus, indicating polystyrene beads escaped from the hot region due to thermophoresis. The effects of laser trapping and convection are negligible compared with thermophoresis of the beads in this setup. Polystyrene beads and typical biomolecules such as DNA migrate to
colder regions at room temperature\textsuperscript{[9]}. However, when we added a small amount of neutral polymer, polyethylene glycol (PEG6000, MW7500, 3.5wt\%) in 10mM Tris buffer, beads and DNA molecules\textsuperscript{[21]} migrated and were trapped at the hot region regardless of the sign of thermophoresis (Fig.1c). The range of attraction reached 5 to 10\(\mu\)m, corresponding to the size of the temperature distribution (see Fig.2a), exceeding by far about 1\(\mu\)m in optical tweezers. As we moved the laser or chamber at several micrometers per second, the trapped polystyrene particles moved with the hot region (see the supporting information \textsuperscript{[22]}). This indicated that the sign and the magnitude of thermophoresis were modified in the presence of polymer under a temperature gradient. This effect was also observed in a bulk heating configuration as shown in Fig.1d (Setup II). Direct absorption of laser light with longer wavelength (1480nm, 25mW, Fujikura) in the water produced a local temperature gradient between thermodiffusion and diffusion as follows.

\begin{equation}
\Delta T_{p} = \frac{-\mu c T}{D_p} \nabla c - c D_p \nabla T,
\end{equation}

where \(c, j_p, D_p, D_T\) are the polymer density, flux, diffusion constant, and thermodiffusion constant, respectively. In the steady state \((j_p = 0)\), the density satisfies

\begin{equation}
dc/c = -(D_T/D_p) dT = -S^P_T dT,
\end{equation}

where the Soret coefficient defined by \(S^P_T = D_T/D_p\) is measured by \(S^P_T = -(1/c)(dc/dT) \approx -\Delta \ln c / \Delta T\). We obtain \(S^P_T = 0.046 \pm 0.005 \text{[K}^{-1}]\) for PEG5000 from the slope in Fig.2(b), in agreement with ref.\textsuperscript{[24]}.



\section*{Trapping Ability.}— Next we examined how the accumulation of beads is dependent on the concentration of polymer and on the local temperature increase by measuring the density distribution of beads. The fluorescence images of beads were recorded for different PEG6000 concentrations. In Fig. 3, spatial distributions of fluorescent polystyrene beads (100 nm, 0.05\%) were displayed. Each image was integrated for 300 frames in 20 seconds and was linearly scaled to 256 grey levels. In 0\% solution, the density decreased from the outer region to the center (Fig.3a). This depletion of beads is explained quantitatively by thermophoresis, as described below. In 1\% solution (Fig. 3b), there was still no trapping, but the degree of depletion is diminished compared to the 0\% solution. In 2\% solution, the trapping phenomenon began to appear and the fluorescence intensity roughly doubled in the hot region (Fig.3c). In the 3.5\% and 5\% solutions, the density increased approximately 10- and 100-fold at the center compared with the surrounding concentrations, respectively (Fig.3d,e).

In Fig.4, the particle density at each distance from the center is plotted against temperature at the same radius (Fig.4). The result for 0\% solution can be described as a steady state distribution due to thermophoresis. The density of beads, \(n\), obeys Eq.\textsuperscript{[3]} with replacement of \(c\) by \(n\) and \(S^p_T\) by \(S^b_T\), where \(S^b_T\) is the Soret coefficient of the beads. Neglecting temperature dependence \(\Delta S^b_T\), an exponential distribution is obtained\textsuperscript{[14]}

\begin{equation}
n = n_0 \exp[-S^b_T (T - T_0)].
\end{equation}

The slope of the curve in Fig.4 gives the Soret coefficient as \(S^b_T = 0.35 \pm 0.03 \text{[K}^{-1}]\) in agreement with previous results\textsuperscript{[9]}. Importantly, even in the presence of polymer, the particle density varied exponentially as a function of the temperature increment (see Fig.4). Therefore a slope of each curves gives an effective Soret coefficient, \(S^*_T\). We plot \(S^*_T\) as a function of PEG concentration in the inset of Fig.4. As a first-order approximation, \(S^*_T\) decreased linearly with the increase of polymer concentration according to the relation

\begin{equation}
S^*_T = S^b_T - \chi c
\end{equation}

with \(\chi = 35.4 \pm 2.0 \text{[K}^{-1}]\) as the best fit, and where \(c\) is the concentration of PEG in weight fraction, or \(\chi = 441 \pm 25 \text{[nm}^3\text{K}^{-1}]\) for \(c\) in volume density. Hence, the sign and the magnitude of the Soret coefficient was controlled by varying the concentration of polymer.

\section*{Theory.}— The main results obtained in our experiment are quantitatively explained by the hydrodynamic theories\textsuperscript{[12,13,14]}. We consider a spherical particle of radius \(a\) in a polymer solution, see the inset of Fig.6. In a dilute regime valid to our experiments, PEG distribution around the particle obeys Boltzmann distribution,
\begin{equation}
\eta \nabla^2 \mathbf{v} = \nabla (p - k_B T \delta c) + f_0(r) \mathbf{e}_z, \tag{5}
\end{equation}

where $f_0(r) \equiv k_B T \bar{c}(S^p_T - 1/T)(1 - e^{-U/k_B T})dT/dz$ and $\bar{c} = c_0(z = 0)$. In Eq. (5), the osmotic pressure, $k_B T \bar{c}$, is compensated by a hydrostatic pressure $p$. (This ensures the absence of osmotic force on the particle proportional to its volume, $\sim k_B T a^3 \delta c$.) The nonequilibrium force, $f_0 \mathbf{e}_z$ in Eq. (5), on the other hand, is balanced with the shear viscous force, $\eta \nabla^2 \mathbf{v}$, leading to a fluid flow relative to the colloid surface and a phoretic motion of the colloid at a velocity $\mathbf{u}$ relative to the fluid at infinity. Solving Eq. (6) in the colloid-reference frame with the no-slip boundary condition, and summing up the resulting fluid stress over the colloidal surface, we obtain the total force acting on the colloid as $\mathbf{F} = -6\pi \eta a \mathbf{u} + 4\pi \varepsilon \mathbf{e}_z \int_a^\infty r(r - a)f_0dr$. This must be zero because no external force is acting on the colloid. Choosing a specific potential of hard-core type (i.e., $U = \infty$ for $a < r < a + \lambda$ and zero otherwise), we finally arrive at

\begin{equation}
\mathbf{u} = \frac{k_B T}{3\eta} (S^p_T - \frac{1}{T}) \lambda^2 \bar{c} \nabla T. \tag{6}
\end{equation}

Plugging then Eq. (6) into an expression of the density current of colloids, $J = n\mathbf{u} - D\nabla n - nD_T \nabla T$\cite{19}, and rewriting it in a form $J = -D\nabla n - nD_S^* \nabla T$, we see that an effective Soret coefficient is given by

\begin{equation}
S^* = S^p_T - 2\pi(S^p_T - \frac{1}{T})a\lambda^2 \bar{c}, \tag{7}
\end{equation}

which confirms the linear dependence on $c$ in Eq. (4), where $\chi = 2\pi(S^p_T - 1/T)a\lambda^2$.

Equation (7) is compared to our experimental data in Fig. 4 inset by employing $S^p_T = 0.056$ for PEG with MW = 7500 estimated from\cite{22}. The best fit gives $\lambda \approx 5.2$ nm, which is close to the PEG gyration radius $\sim 3$ nm\cite{27}. We consider the agreement satisfactory, as $\lambda$ should be of the order of a PEG size. A further consistency check was made by looking at the dependence of $S^*_T$ on the particle radius $a$. To focus only on this dependence of $S^*_T$, we define an effective depletion volume at nonequilibrium $V = \chi/(S^p_T - 1/T)$. First, we performed the series of experiments for four different colloid sizes, and extracted $V$ from the data on $S^*_T$, which are plotted in Fig. 4 as a function of the diameter $2a$. The data shows an overall linear dependence, and the agreement with the theoretical prediction for no-slip condition, $V = 2\pi \lambda^2 a$, obtained from Eq. (7) is good. Note that we used $\lambda = 5.2$ nm obtained before, and thus no adjustable parameter is assumed. Nevertheless, it would be important to examine
and velocity. The parameter $\ell$ defines a slip length on the surface (the no-slip or perfect slip limit is attained for $\ell = 0$ or $\ell = \infty$)\cite{24}. In this Navier case we obtain $V \sim 2\pi a \lambda [a \lambda + 2(\ell + 2\lambda)]/(a + 3\ell)$. This formula, with $\lambda = 1.5$ nm and $\ell = 9.7$ nm as the best fit, actually improves the agreement with the data for $a < 50$ nm, where the deviation from the linear dependence is observable (see Fig. 4). In our system, therefore, a fluid slip might be relevant for $a < 50$ nm (with a relatively large slip length $\ell \sim 10$ nm).

Summary.— We have developed a micro-manipulation technique allowing us to invert and amplify the movement of colloid particles due to thermophoresis of polymers induced by laser focusing. The polymer concentration gradient created by thermophoresis causes migration of a particle with a speed determined by the balance between the driving force and the viscous force. This new method and its application to trapping of molecules based on nonequilibrium effects does not rely on a specific character of particles and polymers, and thus provides further applications for manipulating a diverse range of colloidal particles as well as biological cells and DNA molecules\cite{21,30}. Our technique is also applicable with other water-soluble molecules\cite{31}. We also note that the effect is stronger for PEG with a larger molecular weight at the same monomer concentration as far as it is lower than the overlap concentration.

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[23] The temperature profile in the solution was measured from the intensity profiles of a temperature-sensitive fluorescent dye, 2',7' Bis(2-carboxyethyl)-5(6) carboxyfluorescein (BCECF)\cite{9,14}. The density of PEG molecules was measured by using fluorescently labeled PEG molecules (rhodamin-PEG, MW5000, Nanos).
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We confirmed that polyvinylpyrrolidone (PVP) and sodium polystyrene sulfonate (NaPSS) also work, yet the effect is strongest for PEG.