We report on the study of the spectroscopic properties in Ytterbium–Terbium (Yb\textsuperscript{3+}-Tb\textsuperscript{3+}) co-doped calcium lithium borate (CaLiBO) glasses, with the study’s focus being on the upconversion process. Intensity parameters $\Omega_2, \Omega_4, \Omega_6$ for CaLiBO:Tb\textsuperscript{3+} are determined by the Judd–Ofelt method to be $\Omega_2 = 15.5 \times 10^{-20}$ cm\textsuperscript{2}, $\Omega_4 = 1.90 \times 10^{-20}$ cm\textsuperscript{2} and $\Omega_6 = 3.69 \times 10^{-20}$ cm\textsuperscript{2}. We have also obtained electric-dipole (and magnetic-dipole) radiative transition probabilities, branching ratios, and lifetime for the Tb\textsuperscript{3+}:D\textsubscript{4} and D\textsubscript{3} levels. In addition, an evaluation of the upconversion processes by luminescence and time-resolved spectroscopy were carried out. The upconversion rise and decay times, energy transfer probability from Yb\textsuperscript{3+} to Tb\textsuperscript{3+} ions, and the efficiency of the processes that depopulate the Tb\textsuperscript{3+}:D\textsubscript{4} level after resonantly pumping the Yb\textsuperscript{3+}:F\textsubscript{5/2} level were estimated. Our results showed that a cooperative energy transfer (CET) from two Yb\textsuperscript{3+} ions to one Tb\textsuperscript{3+} ion is the origin of the Tb\textsuperscript{3+} upconversion luminescence in the visible region. While, CET followed of the cross relaxation or/and excited state absorption is responsible for the upconversion luminescence in the ultraviolet region.

Keywords: Judd-Ofelt analysis; cross relaxation or/and excited state absorption; upconversion; CaLiBO glasses; rare earth ions; luminescence.
were obtained using a He-Cd laser (Kimmon/IKS652R-G) at 325 nm as the excitation source. The luminescent signal was dispersed by a monochromator (0.3 m, Thermo Jarrel Ash/82497), detected by a photomultiplier tube (PMT) (Hamamatsu/R928), and amplified by a lock-in amplifier. The UC luminescence spectra were obtained using an InGaAs index-guided strained-layer diode laser (Coherent, 980 nm excitation wavelength) as the excitation source, and the same laser was employed for the excitation power dependent measurements. Tb\textsuperscript{3+}\textsuperscript{3+}:5D\textsubscript{4}\textsuperscript{4} UC luminescence kinetic response measurements were performed using an optical parametrical oscillator (OPO) (Surelite SLOP/Continuum) pumped by the third harmonic (355 nm) of a Nd-YAG laser (Surelite SLII-10/Continuum, 10 Hz, 5 ns) to generate excitation at a wavelength of 980 nm. The signal was dispersed by the same single monochromator (0.3 m) and the Tb\textsuperscript{3+}\textsuperscript{3+}:D\textsubscript{4}\textsuperscript{4}F\textsubscript{4} UC luminescence decay curves were recorded using the PMT and a digital oscilloscope (TekTronix/TDS380) to estimate the Tb\textsuperscript{3+}\textsuperscript{3+}:5D\textsubscript{4}\textsubscript{4} luminescence rise and decay times. All spectroscopic measurements were obtained at room temperature.

RESULTS AND DISCUSSION

Absorption spectra and Judd-Ofelt analysis

Figure 1 presents the absorption spectrum of 1.0Yb+2.0Tb co-doped CaLiBO glass in the 250-1500 nm range. This spectrum is also representative for all the samples. The spectrum presents the typical Tb\textsuperscript{3+}\textsuperscript{3+} bands in regards to line shapes and wavelengths. The electronic levels of Tb\textsuperscript{3+}\textsuperscript{3+}, excited by transitions from F\textsubscript{6} ground state are indicated, as well as the F\textsubscript{5}g→2F\textsubscript{5} transition of Yb\textsuperscript{3+} at 980 nm. The absorption coefficient in the NIR referring to the typical Tb\textsuperscript{3+}\textsuperscript{3+} bands in regards to line shapes and wavelengths. The spectrum is representative for the glasses with different Yb\textsuperscript{3+} doping concentrations, and it is an indication of the successful incorporation of Yb\textsuperscript{3+} ions, for the prepared glass samples (not shown here).

![Figure 1. Room temperature representative ground state absorption spectrum of 1.0Yb+2.0Tb co-doped glass sample. The transitions from ground states F\textsubscript{4} and F\textsubscript{5}g are indicated.](image)

In order to analyze the radiative properties of the Tb\textsuperscript{3+}\textsuperscript{3+} ions, such as the total radiative transition rate between levels, luminescence branching ratios and radiative lifetimes, the well-established Judd-Ofelt (JO)\textsuperscript{4}\textsuperscript{23} theory was applied. The Ω\textsubscript{λ} intensities parameters (λ = 2, 4, 6) are extracted by the experimental and calculated oscillator strengths for each ground state absorption transition.

The experimental oscillator strength is obtained from the absorption spectrum according to the following equation (1):

$$F_{\text{exp}} = \frac{mc}{\pi\epsilon^2 N} \int \alpha(v) dv$$

The oscillator strength calculated contains the reduce matrix element of the given transition, and the Ω\textsubscript{λ} parameters, and is given by the equation (2):

$$F_{\text{cal}} = \frac{8\pi^2 m}{3\hbar} \int \frac{\alpha\lambda(v)}{2J+1} \left( \sum_{J'} \frac{|aJ\lambda|U^\lambda[J'J]|bJ'|^2}{\nu} \right) dv$$

In which $\alpha$ is the average transition energy in cm\textsuperscript{-1} and J is the total angular momentum of the emitting level. The luminescence branching ratios and the radiative lifetime are given by:

$$\beta(aJ; bJ') = \frac{A(aJ; bJ')}{\sum A(aJ; bJ')}$$

and

$$\tau_{\text{rad}} = \frac{1}{\sum aJ\sum A(aJ; bJ')}$$

respectively.

The absorption spectrum obtained for a sample with 2.0Tb was used to obtain the Ω\textsubscript{λ} intensities parameters, where λ = 2, 4, 6 for the CaLiBO glass doped with Tb\textsuperscript{3+}\textsuperscript{3+} ions.

Table 1 presents the experimental and calculated oscillator strengths for the J→J’ absorption transitions from the ground F\textsubscript{6} state to the excited levels, obtained using equations 1 and 2. The root-mean square (RMS) error for oscillator strengths was 1.8%. We determined the intensity parameters Ω\textsubscript{λ} for CaLiBO:Tb\textsuperscript{3+}\textsuperscript{3+}: $\Omega_2 = 15.5 \times 10^{-20}$ cm\textsuperscript{2}, $\Omega_4 = 1.90 \times 10^{-20}$ cm\textsuperscript{2} and $\Omega_6 = 3.69 \times 10^{-20}$ cm\textsuperscript{2}.

The radiative transition rates considering the electric and magnetic dipole contributions, branching ratios and radiative lifetimes of the D\textsubscript{4} and D\textsubscript{3} levels are given in Tables 2 and 3, respectively.

Luminescence

The visible Stokes luminescence spectra were obtained after direct excitation into the D\textsubscript{4} energy level of Tb\textsuperscript{3+} ions at 325 nm. Figure 2 shows the corresponding spectrum for the 1.0Yb+0.5Tb co-doped glass. Regarding the line shape and wavelength positions, this spectrum is representative for the glasses with different Yb\textsuperscript{3+} doping.
The visible Stokes luminescence is reduced by a factor of 2 with an increase in the concentration of Yb\(^{3+}\) ions from (0.1 to 2.5) %mol, and NIR luminescence in the 950-1100 nm range from Yb\(^{3+}\) ions is enhanced nearly 17 times (not shown here). This result is explained by the DC process from Tb\(^{3+}\) to Yb\(^{3+}\), as discussed in our previous article.\(^{20}\) In that work, for the 0.0Yb+0.5Tb single-doped glass, after excitation at 488 nm and monitoring the Tb\(^{3+}:\) 5D\(^4\) level at 544 nm, decay time was significantly higher, 2.38 ms than the Tb\(^{3+}:\) 5D\(^4\) level radiative lifetime, 1.87 ms obtained in this work using Judd-Ofelt calculations (see Table 2). This difference in times could be explained in terms of an energy migration between Tb\(^{3+}\) ions, which induces a lengthening on the 5D\(^4\) emitter level.

### Upconversion emission studies

An analysis of the UC luminescence for the Yb\(^{3+}\)-Tb\(^{3+}\) co-doped CaLiBO glasses with excitation at 980 nm was performed. Figure 3 shows a simplified energy level diagram of the Yb\(^{3+}\) and Tb\(^{3+}\) ions with the relevant optical transitions. The UC through cooperative energy transfer (CET), the Yb\(^{3+}\)-Tb\(^{3+}\) cross-relaxation (CR) and (ESA) excited state absorption processes are indicated by dotted lines. The concentrations. As observed, a dominant green emission band with a peak centered at approximately 544 nm was identified and assigned to the Tb\(^{3+}:\) D\(_{4}\)→F\(_{5}\) emitter level. The Tb\(^{3+}:\) D\(_{4}\)→F\(_{6,4,3}\) emitter levels were also identified with peak emission bands centered at 488, 586 and 622 nm, respectively.
non-radiative relaxation processes, excitation and emission transitions are indicated by dashed, dashed-dotted and solid lines, respectively.

The UC luminescence spectrum of the 1.0Yb+0.5Tb co-doped sample is presented in Figure 4 (a). The position and shape of the emission bands are consistent with those obtained upon direct excitation at 325 nm of the Tb\(^{3+}\):\(^{5}D_{4}\) level (Figure 3). A quadratic dependence on the excitation power at \(\lambda_{ex}=980\) nm was observed in a log-log plot (not shown here) for the UC emission bands associated with the Tb\(^{3+}\):\(^{5}D_{4}\rightarrow^{7}F_{J}\), \(J = 3, 4, 5,\) and 6 emitter levels. This indicates that the absorption of two NIR photons results in the emission of one visible photon, as shown in Figure 3. Is important to mention that the CET process is not resonant. This process is mediated by phonons (thermal energy) to bridge the electronic energy gap between the Tb\(^{3+}\):\(^{3}D_{1}\) level and two the lowest crystal field level of Yb\(^{3+}\):\(^{2}F_{5/2}\).

The dependence of the peak intensity with Yb\(^{3+}\) concentration of the emission band centered at 544 nm (Tb\(^{3+}\):\(^{5}D_{4}\rightarrow^{7}F_{5}\) emitter level) via the UC process is shown in the inset of Figure 4 (a). In this inset, the Tb\(^{3+}\):\(^{5}D_{4}\rightarrow^{7}F_{J}\) UC luminescence increases nearly 68 times, with Yb\(^{3+}\) doping up to 2.5 %mol due to the increase in the number of Yb\(^{3+}\) activator ions; however, there is a quenching in the intensity for higher Yb\(^{3+}\) concentrations (> 2.5 %mol, indicating losses due to the Yb\(^{3+}\)-Tb\(^{3+}\) CR processes (see Figure 3). This is even if the energy transfer probability from Yb\(^{3+}\) to Tb\(^{3+}\), extracted from time-resolved measurements, increases with Yb\(^{3+}\) concentration (as will be shown below). Figure 4 (b) shows the UC luminescence spectra of the xYb+0.5Tb co-doped samples in the UV-blue region (monitoring the \(^{3}D_{1}\) level). The Tb\(^{3+}\):\(^{5}D_{4}\rightarrow^{7}F_{J}\), \(J = 4, 5, 6\) transitions are indicated, and an increase of the UC intensity can be observed. Moreover, the CR and ESA processes (see Figure 3) are confirmed by the curves of UC intensity versus pump power, monitoring the Tb\(^{3+}\):\(^{5}D_{4}\rightarrow^{7}F_{2}\) transition (not shown here). The emission around 440 nm presents a slope coefficient of 3, confirming the three-photon absorption mechanism that excites the Tb\(^{3+}\):\(^{3}D_{1}\) level.

**UC luminescence kinetic response of Tb\(^{3+}\)**

Time-resolved measurements enable the extraction of further information regarding the energy transfer process involved. We attempted to estimate the energy transfer probability from Yb\(^{3+}\) to Tb\(^{3+}\), and the efficiency of the processes that depopulate the Tb\(^{3+}\):\(^{5}D_{4}\) level after resonantly pumping the Yb\(^{3+}\):\(^{2}F_{5/2}\) level. The analysis of the temporal evolution of the luminescence, specifically the rising feature after a short pulse, is a well-known fingerprint of an energy transfer process that does not require light to proceed, and therefore continues after the laser pulse.\(^{10}\) Thus, the Tb\(^{3+}\):\(^{5}D_{4}\rightarrow^{7}F_{J}\) (544 nm) UC luminescence kinetics was studied as a function of the Yb\(^{3+}\) doping concentration. These measurements enable a description of the Tb\(^{3+}\) UC processes.

Figure 5 shows the normalized Tb\(^{3+}\):\(^{5}D_{4}\rightarrow^{7}F_{J}\) (544 nm) UC luminescence kinetics after pumping the Yb\(^{3+}\):\(^{2}F_{5/2}\) level at 980 nm using a 5-ns pulsed laser as excitation source. The inset in Figure 5 shows the first millisecond following the laser pulse. It should be noted that the rise part of the Tb\(^{3+}\):\(^{5}D_{4}\rightarrow^{7}F_{J}\) (544 nm) UC luminescence transient rose slowly from zero intensity after the laser pulse. The rise part of the transient was strongly affected by the Yb\(^{3+}\) concentration. In addition, the decay part of the transient exhibited non-exponential behavior.

The results indicate that the origin of the Tb\(^{3+}\):\(^{5}D_{4}\rightarrow^{7}F_{J}\) (544 nm) UC luminescence is due to a CET process from two Yb\(^{3+}\) ions to one Tb\(^{3+}\) ion. Thus, in accordance with Salley et al.,\(^{27}\) the transients can be fitted using the following equation (6):

\[
I(t) = A \left( e^{-\frac{t}{\tau_1}} - e^{-\frac{t}{\tau_2}} \right)
\]

where \(\tau_1\) and \(\tau_2\) represent the decay and rise times of the transient, respectively. \(\tau_1\) provides information about the radiative and non-radiative process in the acceptor ion and the inverse of \(\tau_2\) provides the energy transfer probability from the donor to the acceptor ion. Note that we have successfully employed equation (6) to estimate the energy transfer probability between Tb\(^{3+}\) and Yb\(^{3+}\) ions in our previous work.\(^{11}\)

Therefore, \(\tau_1\) decreases from 1.64 to 0.79 ms and \(W_{ET}\) increases from 6.7 \(\times\) 10\(^{3}\) s\(^{-1}\) to 45.5 \(\times\) 10\(^{3}\) s\(^{-1}\) with Yb\(^{3+}\) doping in the range of 0.1-7.0 %mol (see Table 4). In the work reported by Terra et al.,\(^{11}\) the mechanisms involved in the UC process in Yb\(^{3+}\)+Tb\(^{3+}\) co-codoped aluminosilicate glasses were analyzed. In that work, the values reported for the UC luminescence rise times are in the range from 20 to 65 microseconds for the temperature range from 123 to 473 K. The inverse of those rise times results in values of probability of energy transfer in the range from 50 \(\times\) 10\(^{-3}\) to 15.4 \(\times\) 10\(^{-3}\) s\(^{-1}\), which are comparable to the values calculated in the present work. On
For comparison purposes, the $\text{Tb}^{3+}:\text{D}_4 \rightarrow \text{F}_5$ (544 nm) decay times after excitation at 488 nm (extracted from our previous DC experiment)\(^20\) are shown in Table 4. Note that these decay times are considerably higher than those estimated in the UC experiment analyzed here. These results indicate that the CR process is present after excitation at 980 nm.

The efficiency of the CR process (Figure 3) that depopulates the $\text{Tb}^{3+}:\text{D}_4$ level after pumping the $\text{Yb}^{3+}:\text{F}_{5/2}$ level could be calculated using the following equation (7):

$$
\eta = 1 - \frac{\tau_{\text{Yb}^{3+}\text{Yb}^{3+}\text{Tb}^{3+}}}{\tau_{\text{Tb}^{3+}}}
$$

where $\tau_{\text{Yb}^{3+}\text{Yb}^{3+}\text{Tb}^{3+}}$ is the $\text{Tb}^{3+}:\text{D}_4 \rightarrow \text{F}_5$ (544 nm) UC luminescence decay time in the presence of $\text{Yb}^{3+}$, and $\tau_{\text{Tb}^{3+}} = 2.38$ ms is the $\text{Tb}^{3+}:\text{D}_4 \rightarrow \text{F}_5$ (544 nm) luminescence decay time for the $\text{Tb}^{3+}$ singly doped sample (0.5 %mol) after excitation at 488 nm (see Ref\(^20\)). These values are summarized in Table 4, where $\eta$ is observed to increase from 31% to 67% when the concentration of $\text{Yb}^{3+}$ ions increases, indicating that the CR process is efficient.

We have observed that the $\text{Tb}^{3+}$ UC luminescence slowly rises over time in our samples. The origin of the $\text{Tb}^{3+}$ UC luminescence is due to a CET process in which two $\text{Yb}^{3+}$ ions simultaneously transfer the energy to one $\text{Tb}^{3+}$ ion ($2\text{Yb}^{3+}:\text{F}_{5/2} ; \text{Tb}^{3+}:\text{F}_{5/2}$; $\text{Tb}^{3+}:\text{D}_4$), as depicted in Figure 3.

**CONCLUSIONS**

This paper presents a qualitative and quantitative perspective on the study of the spectroscopic properties of $\text{Yb}^{3+}$-$\text{Tb}^{3+}$ co-doped CaLiBO glasses, using absorption, luminescence and time-resolved measurements. Intensity parameters $\Omega$ for CaLiBO: $\text{Tb}^{3+}$ glass have been determined by the Judd–Ofelt method to be $\Omega_1 = 15.5 \times 10^{-20}$ cm$^2$, $\Omega_2 = 1.90 \times 10^{-20}$ cm$^2$ and $\Omega_3 = 3.69 \times 10^{-20}$ cm$^2$. These values were used to calculate spectroscopic properties, such as oscillator strengths, probabilities, and radiative lifetimes. The analyses covered herein showed that CaLiBO glass is a good host for high concentrations of $\text{Yb}^{3+}$ and $\text{Tb}^{3+}$ ions. The rise and decay times of the $\text{Tb}^{3+}:\text{D}_4 \rightarrow \text{F}_5$ UC transient luminescence allowed for determination of the energy transfer probability and the efficiency of the processes that depopulate the $\text{Tb}^{3+}:\text{D}_4$ level after resonantly pumping the $\text{Yb}^{3+}:\text{F}_{5/2}$ level. The time-resolved measurements identified the origin of the $\text{Tb}^{3+}:\text{D}_4 \rightarrow \text{F}_5$ UC luminescence as a cooperative energy transfer mechanism from two $\text{Yb}^{3+}$ ions to one $\text{Tb}^{3+}$ ion. The results suggest that $\text{Yb}^{3+}$-$\text{Tb}^{3+}$ co-doped CaLiBO glasses are potential materials for applications in the form of optical converters.

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