Sterile neutrino portal to Dark Matter II: exact dark symmetry

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Abstract We analyze a simple extension of the standard model (SM) with a dark sector composed of a scalar and a fermion, both singlets under the SM gauge group but charged under a dark sector symmetry group. Sterile neutrinos, which are singlets under both groups, mediate the interactions between the dark sector and the SM particles, and generate masses for the active neutrinos via the seesaw mechanism. We explore the parameter space region where the observed Dark Matter relic abundance is determined by the annihilation into sterile neutrinos, both for fermion and scalar Dark Matter particles. The scalar Dark Matter case provides an interesting alternative to the usual Higgs portal scenario. We also study the constraints from direct Dark Matter searches and the prospects for indirect detection via sterile neutrino decays to leptons, which may be able to rule out Dark Matter masses below and around 100 GeV.

1 Introduction

Dark Matter and neutrino masses provide experimental evidence for physics beyond the standard model (SM), and finding a scenario where both phenomena are linked is an exciting possibility. Another hint to a connection between these two sectors comes from the standard mechanisms to generate the Dark Matter relic abundance and neutrino masses, as both seem to require new massive degrees of freedom, with a thermal relic and right-handed neutrinos, respectively.

An obvious possibility would be for right-handed neutrinos to constitute the Dark Matter of the Universe [1]. This option is constrained to a specific region at the keV and small mixing with active neutrinos in the minimal see saw model, but in extended scenarios a larger parameter space is allowed, for instance in the context of a gauged $B−L$ symmetry [2,3]. Upcoming experiments may be able to exclude or establish whether keV neutrinos are the origin of Dark Matter, see e.g. [4].

In this paper we take a different approach, focusing on the fact that heavy neutrinos can mediate between Dark Matter and the SM. We propose a simple extension of the SM with a new scalar and fermion, singlets under the SM gauge group but charged under a dark sector symmetry group. Sterile neutrinos, which are singlets under both groups, are able to mediate the interactions between the dark sector and the SM particles, as well as generate masses for the active neutrinos via the seesaw mechanism. Therefore, the same coupling that generates neutrino masses after electroweak symmetry breaking, determines the Dark Matter phenomenology. Indeed, Dark Matter annihilation to right-handed neutrinos and subsequent decays to SM particles characterize the computation of the relic abundance as well as indirect detection probes, respectively.

This minimal set-up has been studied in [5,6] for the case of fermion Dark Matter, under the assumption that the sterile neutrinos are pseudo-Dirac and heavier than the dark sector particles. Our analysis differs from this previous work in that: (1) we explore the region of parameter space where sterile neutrinos are lighter than the dark sector, and therefore the Dark Matter can annihilate into sterile neutrinos and (2) we extend the analysis to the scalar Dark Matter case, which was not considered before.

In a companion paper [7], we have explored an alternative scenario with the dark sector charged under $U(1)_{B−L}$, and both papers provide two distinct possibilities for a sterile neutrino portal to Dark Matter.

The paper is organized as follows. After presenting the set-up of our model in Sect. 2, we move onto the constraints from Higgs decays and direct Dark Matter searches in Sect. 3. We describe the calculation of the annihilation cross section in Sect. 4 where we impose constraints from the relic abundance of Dark Matter. These results are then linked to indirect detection probes via sterile neutrinos decays to leptons...
in Sect. 5. We conclude in Sect. 6 by summarizing our main findings.

2 Exact dark symmetry

This portal is based upon the assumption that the dark sector contains at least a scalar field \( \phi \) and a fermion \( \Psi \), which are both singlets of the SM gauge group but charged under a dark sector symmetry group, \( G_{\text{dark}} \), so that the combination \( \overline{\Psi} \phi \) is a singlet of this hidden symmetry. Independently of the nature of the dark group, if all SM particles as well as the sterile neutrinos are singlets of \( G_{\text{dark}} \), the lighter of the two dark particles turns out to be stable, and therefore it may account for the Dark Matter density of the Universe.

If this were the case then nothing would prevent a term like

\[
\mathcal{L}_{\text{int}} = -(\phi \overline{\Psi} (\lambda_s + \gamma \lambda_p) N + \phi^\dagger \overline{N} (\lambda_s - \gamma \lambda_p) \Psi)
\]

(1)

to appear, besides the standard Higgs portal term \( \lambda \overline{H} \overline{H}^\dagger H \) included in the scalar potential,

\[
\mathcal{L}_{\text{scalar}} = \mu_H^2 \overline{H}^\dagger H - \lambda_H \overline{H}^\dagger H \overline{H} \overline{H} - \mu_\phi^2 \phi^\dagger \phi - \lambda_\phi \phi^\dagger \phi^\dagger \phi
\]

(2)

and the term responsible for the generation of neutrino masses

\[
\mathcal{L}_{\nu N} = -(Y_{\alpha a} \overline{T_a} H N_{Ra} + h.c.),
\]

(3)

where \( \alpha = e, \mu, \tau \) denotes lepton flavour and \( a = 1 \ldots n \), being \( n \) the number of sterile neutrinos.

For simplicity we do not consider the possibility that the scalar \( \phi \) gets a vev, and we restrict the discussion to the minimal matter content, although there could be more than one set of dark fermions and scalars.

Another simplifying assumption made in this paper is that the dark symmetry \( G_{\text{dark}} \) is a global symmetry at low energies. We are therefore neglecting the possible phenomenology of \( G_{\text{dark}} \) vector mediators, e.g., if the dark symmetry was local there could also be kinetic mixing among the dark gauge bosons and the SM ones, leading to further SM-dark particle interactions [8,9]. The following discussion will apply as well to this scenario, provided the kinetic mixing is negligible. Nevertheless, the UV structure and stability of Dark Matter depends on whether \( G_{\text{dark}} \) is a true global symmetry or a gauge symmetry. Global symmetries are sensitive to higher-dimensional operators mediated by quantum gravity effects [10], e.g. \( c_\phi \overline{\Psi} \overline{H}^\dagger \gamma^\mu D_\mu L \overline{M}_P \) or \( c_\phi \Phi F_{\mu \nu} F^{\mu \nu} / M_P \), and could lead to disastrous decay of Dark Matter unless \( c_\phi \Phi \ll 1 \) [11–13].

Regarding the neutrino sector, light neutrino masses are generated via TeV scale type I seesaw mechanism, which we briefly review in the following. We denote \( \nu_a \) the active neutrinos and \( N_s \) the sterile ones. After electroweak symmetry breaking, the neutrino mass matrix in the basis \((\nu_a, N_s)\) is given by

\[
\mathcal{M}_\nu = \left( \begin{array}{cc} 0 & m_D \end{array} \right),
\]

(4)

where \( m_D = Y v_H / \sqrt{2} \) and \( Y_{\alpha s} \) are the Yukawa couplings.

The matrix \( \mathcal{M}_\nu \) can be diagonalized by a unitary matrix \( U \), so that

\[
\mathcal{M}_\nu = U^* \text{Diag}(m_\nu), \quad \nu_i = U^* \begin{pmatrix} \nu_a \\ N_s \end{pmatrix}.
\]

(5)

The unitary matrix \( U \) can be written as

\[
U = \begin{pmatrix} U_{ai} & U_{ah} \\ U_{si} & U_{sh} \end{pmatrix},
\]

(6)

where, at leading order in the seesaw expansion parameter, \( O(m_D / m_N) \):

\[
U_{ai} = [U_{\text{PMNS}}]_{ai}, \quad U_{sh} = I,
\]

(7)

\[
U_{ah} = [m_D m_N^{-1}]_{ah}, \quad U_{si} = -[m_N^{-1} m_D U_{\text{PMNS}}]_{si}.
\]

Notice that at this order the states \( N_h \) and \( N_s \) coincide, so we identify them in the rest of this paper.

Neglecting the mixing between the CP-even scalars, the Yukawa coupling of the SM-like Higgs field \( h \) to the neutrinos can be written as [14]:

\[
\mathcal{L}_Y = \frac{h}{2v_H} \overline{\nu}_i [(m_i + m_j) \text{Re}(C_{ij}) + i \gamma_5 (m_j - m_i) \text{Im}(C_{ij})] n_j,
\]

(8)

where the indices \( i, j \) refer to the light neutrinos \( \nu_i \) for \( i, j = 1, 2, 3 \) and to \( N_h \) for \( i, j = 4, 5, 6 \), and the matrix \( C \) can be written in terms of the mixing matrix \( U \):

\[
C_{ij} = \sum_{a=1}^{3} U_{ai} U_{aj}^*,
\]

(9)

A variation of this scenario has been analyzed in [5,6], where the sterile neutrinos are assumed to be pseudo-Dirac and...
heavier than the dark sector particles, $\phi$, $\Psi$. Thus, they can be integrated out and generate at tree level the effective dimension five operator

$$\mathcal{O}^{(5)} = (\bar{\Psi} \phi)(\bar{H}^\dagger \ell),$$

which after the SM Higgs doublet acquires a vev leads to the interaction $\mathcal{O}^{(5)} = (\bar{\Psi} \phi) v_L v_H / \sqrt{2}$, involving a SM left-handed neutrino. This limit is in fact a (light) neutrino portal to Dark Matter. Assuming that the fermion $\Psi$ is the Dark Matter, the model can accommodate current experimental and observational constraints if $M_\phi$ is below $\sim 35$ GeV, or it is in a resonant region of the Higgs or $Z$ boson, or the dark scalar and dark fermion are almost degenerate.

Our analysis is complementary, since we focus on a different region of the model parameter space: we assume that the sterile neutrinos are lighter than the Dark Matter and therefore the annihilation channel to $NN$ is open. Furthermore, we study both fermion and scalar Dark Matter. Although the scalar Dark Matter case falls among the class of Higgs portal models that have been extensively studied \cite{ref15--34}, it is worth to explore whether the new annihilation channel into $NN$ allows one to obtain the observed relic density in regions that are excluded in the standard Higgs portal framework.

In the following sections we describe the current constraints on the above scenario and the results of our numerical analysis, based on a Monte Carlo scan over the free parameters $(m_\psi, m_\phi, m_N, \lambda_s, \lambda_{H\phi})$ in logarithmic scale, restricting the values of the masses and couplings to the ranges displayed in Table 1. We present the analytic results for arbitrary Dark Matter—sterile neutrino couplings $\lambda_s, \lambda_p$, but for the numerical implementation we have chosen $\lambda_p = 0$, since as explained in Sect. 4, in this case strong constraints can be set from indirect Dark Matter searches. We made use of LanHep \cite{ref35} and micrOMEGAs \cite{ref36} in order to obtain the correct relic abundance, Higgs decays and today’s annihilation cross section. We calculate $10^6$ points that match the Planck constraint on the Dark Matter abundance at $3\sigma$ \cite{ref37}, namely $\Omega h^2 = 0.1198 \pm 0.0045$.

### Table 1 Explored parameter space in the models

| Case         | $m_\psi$ (GeV) | $m_\phi$ (GeV) | $m_N$ (GeV) | $\lambda_s$ | $\lambda_{H\phi}$ |
|--------------|----------------|----------------|-------------|--------------|-------------------|
| Fermion DM   | $1\sim 2 \times 10^3$ | $1\sim 10^4$ | $1\sim 2 \times 10^3$ | $10^{-4} \sim -4\pi$ | $10^{-4} \sim -4\pi$ |
| Scalar DM    | $1\sim 10^3$ | $1\sim 2 \times 10^3$ | $1\sim 2 \times 10^3$ | $10^{-4} \sim -4\pi$ | $10^{-4} \sim -4\pi$ |

3 Constraints from Higgs decays and direct Dark Matter searches

The enlarged fermion and scalar sectors lead to new decays of the Higgs boson, $h$, which can be constrained using the ATLAS and CMS limits on the invisible Higgs decay branching fraction:

$$BR_{inv} = \frac{\Gamma_{inv}}{\Gamma_{inv} + \Gamma_{SM}} < 0.23 \quad (95\% \text{ CL}),$$

(12)

being the SM Higgs width $\Gamma_{SM} \approx 4$ MeV.

At tree level, there are two new Higgs decay channels: when $m_\phi < m_h/2$, the standard decay of the Higgs portal scenarios, $h \rightarrow \phi \phi$ is kinematically allowed, contributing to the invisible Higgs decay width by

$$\Gamma(h \rightarrow \phi \phi) = \frac{\lambda^2_{H\phi} v_H^2}{8\pi m_h} \left[ 1 - \frac{4m_\phi^2}{m_h^2} \right].$$

(13)

We show in Fig. 3 the upper limit on the Higgs portal coupling $\lambda_{H\phi}$ derived from the experimental limit on the invisible Higgs decay width in Eq. (12), as a function of the singlet scalar mass, $m_\phi$.

Moreover, the Yukawa interaction term $Y_{TH} H P_R N$ also leads to novel Higgs decay channels into neutrinos. The corresponding decay width reads \cite{ref14}:

$$\Gamma(h \rightarrow n_i n_j) = \frac{\omega}{8\pi m_h} \lambda^{1/2}(m_i^2, m_j^2)$$

$$\times \left[ S \left( 1 - \frac{(m_i + m_j)^2}{m_h^2} \right) + P \left( 1 - \frac{(m_i - m_j)^2}{m_h^2} \right) \right],$$

(14)

where $\lambda(a, b, c)$ is the standard kinematic function, $w = 1/n!$ for $n$ identical final particles and the scalar and pseudoscalar couplings are:

$$S = \frac{1}{v_H^2} \left[ (m_i + m_j)^2 \text{Re}(C_{ij}) \right]^2,$$

$$P = \frac{1}{v_H^2} \left[ (m_j - m_i)^2 \text{Im}(C_{ij}) \right]^2,$$

(15)

with $C_{ij}$ defined in Eq. (10).

The largest branching ratio is for the decay into one light and one heavy neutrino \cite{ref38}:

$$\Gamma(h \rightarrow vN) = \frac{m_N^2}{8\pi v_H^2} \left( 1 - \frac{m_h^2}{m_N^2} \right)^2 m_h |C_{vN}|^2.$$

(16)

The attainable values for the above branching fractions have been analyzed in \cite{ref38}, for the case of two heavy neutrinos, parameterizing the Yukawa couplings in terms of the observed light neutrino masses and mixing angles, and a
complex orthogonal matrix. After imposing the relevant constraints from neutrinoless double beta decay, lepton flavour violating processes and direct searches of heavy neutrinos, they find that branching ratios of $h \rightarrow \nu_i$ Na larger than $10^{-2}$ are generally ruled out for heavy neutrino masses $M_N \leq 100$ GeV, and typically they are much smaller, due to the tiny Yukawa couplings required to fit light neutrino masses with sterile neutrinos at the electroweak scale. Therefore, the contribution of such decay modes to the Higgs decay width is negligible, and they do not alter the bounds discussed above.

At one loop, the $d = 5$ Higgs portal operator $\bar{\Psi} \Psi (H^\dagger H)$ is generated (unless the coupling of the Dark Matter to the dark scalar and sterile neutrinos is chiral, i.e., $\lambda_s = \lambda_p$ in Eq. (1)) with a coefficient given by [6]:

$$\lambda_{H\Psi}^{\text{eff}} = \frac{(\lambda_s^2 - \lambda_p^2)}{16\pi^2} \frac{m_N}{(m_N^2 - m_N^2)^2} \times \left( m_N^2 - m_N^2 + m_N^2 \log \frac{m_N^2}{m_N^2} \right).$$

(17)

Thus, when $m_\Psi < m_h/2$ the invisible decay $h \rightarrow \Psi \Psi$ is also allowed with partial decay width

$$\Gamma(h \rightarrow \Psi \Psi) = \frac{(\lambda_{H\Psi}^{\text{eff}})^2}{8\pi} \left( 1 - \frac{4m_\Psi^2}{m_h^2} \right)^{3/2} m_h.$$  

(18)

and the current limit on the invisible Higgs decay branching ratio only leads to an $O(1)$ constrain on $\lambda_{H\phi}$, depending on the values of the remaining free parameters, namely $\lambda_s$, $\lambda_p$, $m_N$ and $m_\phi$. Notice, however, that if $m_\phi < m_h/2$, the strong constraints from the invisible Higgs decay $h \rightarrow \phi \phi$ shown in Fig. 3 will apply as well.

Concerning the bounds from direct DM searches, they also depend on which of the dark particles is lighter, and therefore stable. In order to implement such bounds we shall assume that the DM relic density is as determined by CMB measurements, since this requirement is always fulfilled in our scenario for both scalar and fermion DM, as we will see in the next section.

If DM is the dark fermion, $\Psi$, it only interacts with the SM quarks at one-loop level (see Fig. 1), via the induced Higgs portal operator $\bar{\Psi} \Psi (H^\dagger H)$ just discussed, and therefore the bounds from direct detection are quite weak. However, since the interaction to quarks is mediated through the Higgs, the scattering will always be spin independent. We refer the reader for the actual matrix elements to [39]. In Fig. 2 we show the excluded region by the invisible Higgs decay and current LUX [40,41] results (dark blue points), as well as the expected excluded region by XENON1T [42] (light blue) and LZ [43,44]+SuperCDMS [45] (purple). Similar constraints can be set with the current results from the PANDAX experiment [46].

**Fig. 1** Left, right elastic cross section diagrams for the scalar and fermion Dark Matter cases, respectively.

**Fig. 2** Constraints on the Higgs portal coupling for fermion DM.
However, if DM is the dark scalar \( \phi \), it interacts with the SM quarks at tree level via the Higgs portal coupling, \( \lambda_{H\phi} \), and the null results from direct searches set strong limits on this parameter. This is illustrated in Fig. 3, where we show the allowed values of the Higgs portal coupling \( \lambda_{H\phi} \) as a function of the DM mass, \( m_\phi \), derived from the invisible Higgs decay width plus LUX bounds, as well as the prospects from XENON1T and LZ+SuperCDMS. The dark blue points in the usual Higgs portal scenario would be ruled out, except for the upper limit, since the \( \lambda_{H\phi} \) being too small leads to a DM relic density larger than the one determined by CMB measurements. In our scenario the alternative annihilation channel into \( NN \) provides the correct relic density, but the current constraints from LUX and Higgs invisible decay width excludes them. We notice that for \( m_\phi \gtrsim 300 \text{ GeV} \) the usual Higgs portal model still provides the correct relic abundance. However, we find that XENON1T can be sensitive to such scenario for \( m_\phi < 2 \text{ TeV} \).

### 4 Dark Matter relic abundance

#### 4.1 Thermal history

In order to discuss the thermal production of Dark Matter in the early Universe we will first describe the thermal history for both the scalar and fermion Dark Matter scenarios.

1. Fermion Dark Matter \( \Psi \): At very early times \( \phi, \Psi \) and \( N \) are in thermal equilibrium with the standard model via the Higgs portal coupling. The heavy dark particle companion will decay at \( T \lesssim m_\phi \) and the dark sector may still be coupled to the standard model bath if the Yukawa couplings of the sterile neutrinos are large enough. If they are small, then the \( \Psi \) and \( N \) bath will decouple and remain in thermal equilibrium but with a different temperature. Then when the temperature of such a bath is \( T_D \sim m_\phi/20 \) the Dark Matter will be produced and the sterile neutrinos will decay at \( T_D \lesssim m_N \). In order to check whether the decoupling of the dark sector will modify the production rate it is worth revisiting the production mechanism, see [47] for a recent discussion of decoupled dark sectors. Since the entropy is separately conserved in both the visible and the dark sectors, the standard relic abundance solution is modified approximately by a factor \( \sqrt{g_\text{eff}^\text{SM}}/g_* \) where \( g_* \) measures the total number of relativistic degrees of freedom in the SM bath and \( g_\text{eff}^\text{SM} = g_* + g_D(T_D/T)^4 \) represents the effective number of relativistic species. Given that the number of degrees of freedom in the dark sector, \( g_D \) is much smaller than \( g_* \) and \( T_D/T \sim 1 \) then \( \sqrt{g_\text{eff}^\text{SM}}/g_* \) must be close to one. Thus, a sizeable change in the couplings compared to the case in which both sectors remain in thermal equilibrium is not expected since furthermore \( \Omega_\chi h^2 \propto 1/\lambda_{4,\phi}^4 \).

The only caveat to this argument occurs when \( m_\chi \gtrsim m_N \), because in that case the sterile neutrinos may have a larger number density than the equilibrium one and in order to generate the same amount of Dark Matter higher couplings between \( \chi \) and \( N \) will be needed. This scenario has been recently studied by [48] for the precise model proposed in this work. They found that in such region one will need couplings a factor between 1 and 4 higher depending on the Yukawa of the sterile neutrinos. Since this change is mild, for our computations we will assume that all species are equilibrium with the standard model.

2. Scalar Dark Matter \( \phi \): At very early times \( \phi, \Psi \) and \( N \) are in thermal equilibrium with the standard model via the Higgs portal coupling. The heavy dark particle companion will decay at \( T \lesssim m_\phi \) and the dark sector will decouple from the standard model when the Dark Matter freezes out at \( T \sim m_\phi/20 \) and the sterile neutrinos will decouple and decay at \( T \lesssim m_N \).

#### 4.2 Relic abundance

In our scenario, the annihilation cross section into two sterile neutrinos depends on the nature of the DM particle (scalar, Dirac or Majorana fermion) and the type of coupling (scalar, pseudoscalar). The relevant Feynman diagrams are shown in Fig. 4. For example, let us assume right-handed neutrinos are Majorana, and consider the two options of fermion and scalar Dark Matter:

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1 Yet, the actual value of the Yukawa couplings are not known. The naive seesaw expectation is \( Y \sim \sqrt{m_{\nu} m_N}/v_H \sim 4 \times 10^{-8}\sqrt{m_N/(1 \text{ GeV})} \) for \( m_\nu \sim 0.1 \text{ eV} \), but larger couplings are consistent with neutrino masses, for instance in the context of inverse seesaw scenarios.
1. Fermion Dark Matter $Ψ$: The cross section for fermionic Majorana Dark Matter and complex mediator $φ$ reads

$$\sigma v_{ΨΨ→NN} = \frac{(α + β r_{NΨ})^2}{4π m_Ψ^2} \sqrt{1 - r_{NΨ}^2} + \mathcal{O}(v^2)$$

where $α = λ_s^2 - λ_p^2$ and $β = λ_s^2 + λ_p^2$, $r_φ = m_φ/m_Ψ$, and $r_{NΨ} = m_N/m_Ψ$.

One can obtain the case of a Dirac DM particle by in Eq. (19) perform the exchange $α ↔ β$. Similarly, the case of a real scalar can be obtained by setting $λ_p = 0$ in Eq. (19), which leads to $α = β = λ_s^2$ in this expression.

2. Scalar Dark Matter $φ$: In the case of a real scalar Dark Matter and Dirac mediator $Ψ$ the cross section is as follows:

$$\sigma v_{φφ→NN} = \frac{(α + β r_{NΨ})^2}{2π m_φ^2} \frac{(1 - r_{NΨ}^2)^{3/2}}{(1 + r_φ^2 - r_{NΨ}^2)^2} + \mathcal{O}(v^2).$$

where $r_φ = m_φ/m_Ψ$ and $r_{NΨ} = m_N/m_Ψ$.

To obtain the expression for a complex scalar, one can multiply this equation by a factor $1/4$. Similarly, to consider a Majorana mediator one would multiply the expression by a factor 4 and set $λ_p$ to zero, $α = β$.

An important observation is that there are situations where the annihilation cross section at leading order in the relative Dark Matter velocity, $v$, is proportional to the right-handed neutrino mass. For example, the case of a Majorana Dark Matter with chiral couplings, $|λ_s| = |λ_p| (α = 0)$. In this case when $m_N \ll m_φ$, $m_φ$ the cross section is effectively p-wave, which reduces the sensitivity of indirect detection probes to these scenarios.

In the following we discuss two representative cases where strong constraints can be set on the parameter space of the sterile neutrino portal, namely cases where the cross section is s-wave even for $m_N = 0$. We choose two benchmark scenarios, namely Majorana DM and real scalar DM with scalar couplings $α = β = λ_s^2$. In Fig. 5 we show the allowed parameter space in the mass of the mediator versus coupling, $λ_s$. Besides the perturbativity limits, the coupling $λ_s$ is constrained by the width of the mediator. In our approach, the mediator particle is treated as a narrow resonance, i.e. $Γ/m \ll 1$, which implies $λ_s \lesssim \sqrt{8π}$. Taking into account this limit, these plots show that the mass of the mediator must be below $m \lesssim 1$ TeV to satisfy $Γ \lesssim 0.1m$.

In the scalar Dark Matter case, annihilation into right-handed neutrinos (Eq. (20)) is complemented via the Higgs portal coupling $λ_Hφ$ into SM particles. Namely $b\bar{b}$ for low mass DM, and gauge bosons and Higgses for heavier DM particles. These channels could, in principle, compete with the annihilation into right-handed neutrinos, yet in Fig. 3 we showed how couplings to SM are strongly constrained by direct detection experiments (LUX) and LHC bounds on the

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Note that our results agree with the expressions obtained in Ref. [49], where both fermions were set to be Dirac particles.
Finally, in the fermion Dark Matter case, since the coupling to the Higgs is generated at 1-Loop, the contributions to the annihilation cross section from the SM particles is only non-negligible in the resonant region \( m_\phi \simeq m_h/2 \).

5 Constraints from indirect searches and CMB

In this scenario the annihilation of Dark Matter (with \( m_{DM} \lesssim 100 \text{ GeV} \)) into right-handed neutrinos is dominant, with the heavy neutrinos decaying into SM particles via their mixing with active neutrinos. Those decays can lead to significant fluxes of gamma rays and neutrinos which can be probed by experiments. In this section we consider the impact on the model by limits from Fermi-LAT and H.E.S.S. on the gamma-ray flux from dwarf spheroidal galaxies [50] and the galactic center [51] respectively, as well as from studies of the CMB [52] and IceCUBE analysis of neutrino fluxes [53–55].

To study the indirect detection signals in this model we first need to understand how the heavy neutrino decays. If the neutrino is light, \( m_N < m_\nu \), \( N \) will mostly decay through off-shell \( Z \) and \( W \). These three-body partial widths can be read from Refs. [56,57] and are listed in the appendix; here we just quote the typical form it adopts:

\[
\Gamma(N \to 3 f) \approx \frac{G_F^2}{192 \pi^3} |U_{Nf}|^2 m_N^5,
\]

where \( U_{Nf} \) is the mixing matrix between the heavy and active neutrinos. For heavier \( N \), the two-body decays into massive vector bosons or Higgs and fermions are open. In this case the partial width scales as [14]:

\[
\Gamma(N \to V f) \approx \frac{g^2}{64 \pi m_{V,Z,h}^2} |U_{Nf}|^2 m_N^3.
\]

See also the appendix for the detailed formulae.

The relative weight of the different lepton flavours to the total width depends on the model for neutrino mass generation. The large angle \( \theta_{23} \) in the active neutrino mixing matrix \( U_{PMNS} \) suggests a similar decay rate of \( N \) into \( \mu \) and \( \tau \), while the one into \( e \) is largely unconstrained. In fact, the measured mixing pattern (see for instance [58]) is close to Tri-Bimaximal, which leads to an exact \( \mu - \tau \) symmetry [59]. In our case, if we assume that the largest active neutrino mass is generated by only one of the sterile neutrinos, \( m_3 \approx \sum_a (Y_{aN} v_H)^2/m_N \) and the mixing angles are given by \( Y_{aN} \sim Y_{aN} v_H/m_N \). Then \( \tan \theta_{23} \sim Y_{\mu N}/Y_{\tau N} \sim 1 \) and \( \tan \theta_{13} \sim Y_{e N}/\sqrt{Y_{\mu N}^2 + Y_{\tau N}^2} \sim 0.15 \) imply that \( U_{eN} \ll U_{\mu N} \approx U_{\tau N} \) [60].

Footnote 3 continued

3 The features in the low mass region of the plots are due to the fact that the contributions to the SM are mediated by the Higgs and there are several suppressions. When different channels become non-negligible in the resonant region \( m_\phi \simeq m_h/2 \).
A detailed study of the indirect detection signatures of our scenario is beyond the scope of this work, since DM does not decay directly to SM particles, as is usually assumed in most analyses. Therefore we just estimate here the expected constraints using current analysis, taking into account that in general the cascade decays lead to a softer energy spectrum of the final SM particles than in the standard two-body decay. In Fig. 7 we present the results of such an estimate exercise in the case of decays to leptons, where limits from Refs. [50,51] have been naively re-scaled as $m_{DM} \rightarrow m_{DM}/2$. We find that decays of the right-handed neutrinos resulting in tau-leptons, e.g. from $N \rightarrow \tau q q'$ or $N \rightarrow \nu \tau^+ \tau^-$, are potentially the most sensitive modes. Indeed, if these decays were dominant one could obtain a limit from indirect detection on the Dark Matter mass of $\mathcal{O}(100)$ GeV for both fermion and scalar Dark Matter. One could also use the production of quarks from off-shell $W$ and $Z$ to set bounds on the model.

Note that indirect detection signals in this case (i.e., $m_N < m_W$) have been studied in [61], showing that it could be possible to explain the galactic center gamma-ray excess revealed by various studies of the Fermi-LAT data in 1–4 GeV gamma rays. Indeed, assuming that DM particles annihilate into two sterile neutrinos lighter than the $W$ boson, they find that $m_N$ in the range 10–60 GeV can explain the observed spectrum, while the fitted annihilation cross section $\sigma v$ is $(0.5–5) \times 10^{-26}$cm$^3$/s, roughly compatible with the WIMP annihilation cross section $\langle \sigma v \rangle_{\text{decouple}} \sim (2 – 3) \times 10^{-26}$cm$^3$/s, when the Dark Matter particles decouple. More precisely, the best fit points are around $m_N \sim 30$ GeV and $m_{DM} \sim 45$ GeV, which are within the ranges we have found compatible with all current experimental constraints in our model.

Finally, let us mention other sources of indirect constraints for this model. Measurements of the cosmic microwave background (CMB) anisotropies are also sensitive to Dark Matter annihilation during the cosmic dark ages, because the injection of ionizing particles will increase the residual ionization fraction, broadening the last scattering surface and modifying the anisotropies. Under the assumption that the power deposited to the gas is directly proportional to that injected at the same redshift, with some efficiency factor $f_{\text{eff}}$, constraints can be placed on the combination $f_{\text{eff}} \langle \sigma v \rangle/m_{DM}$, for different SM annihilation channels in $s$ wave. Again, the available calculations of $f_{\text{eff}}$ assume that DM annihilates directly to a pair of SM particles [52], and thus they are not directly applicable to our model, but we can roughly estimate the expected impact of such limits in the allowed parameter space assuming as before that the constraints will be similar for cascade decays, appropriately re-scaled for $m_{DM}/2$. Under these circumstances, we find these limits are weaker than the ones from Fermi-LAT discussed above.

Besides signatures from gamma rays, in the $NN$ annihilation channel also light neutrinos are copiously produced, which could generate an observable flux from dense regions of Dark Matter. IceCUBE has set constraints on the Dark Matter annihilation cross section to neutrinos by measuring the flux from nearby Galaxies and Clusters [53], the Galactic Halo [54] and the Galactic Center [55]. However, currently these probes lie three orders of magnitude above the model prediction, and thus cannot place a constrain on our model.

Dark Matter particles in the galactic halo can also scatter elastically with a nucleus and become trapped in the gravitational well of astronomical objects like the Sun, eventually thermalize and concentrate at the core of the object. Then they may annihilate into SM particles, in particular neutrinos that can be detected by neutrino experiments such as IceCUBE or SuperKamiokande. In our scenario the limits from direct searches are tighter than such indirect probes, since the interaction of Dark Matter to quarks is spin independent.

6 Conclusions and outlook

In this paper we have analyzed in detail a simple scenario of a dark sector composed of a scalar and a fermion, both singlets under the SM gauge group but charged under a dark symmetry group. This sector is linked to the origin of neutrino masses via couplings to the sterile neutrinos, which are able to mediate between the dark sector and the SM.
This scenario has been studied in Refs. [5,6], considering just the case of fermionic Dark Matter and for sterile neutrinos heavier than the dark sector, with the result that current experimental and observational constraints (electroweak precision limits, Dark Matter relic abundance, direct and indirect detection constraints), can be accommodated only for \( m_{\text{DM}} \lesssim 35 \text{ GeV} \), or in the resonances, \( m_{\text{DM}} \simeq m_h, m_Z \), unless the dark scalar or dark fermion are almost degenerate.

We have extended these previous studies in two ways: we explore the phenomenology of this type of models when the sterile neutrinos are lighter than the dark sector, so that the Dark Matter annihilation channel into \( NN \) is kinematically allowed, and we consider both, fermionic and scalar Dark Matter in this context. We have performed for the first time an exhaustive numerical analysis of this alternative region of the model parameter space, and after imposing all the relevant constraints from direct detection and collider probes, we find that it is possible to obtain the observed Dark Matter relic abundance in the whole mass range explored, \( m_{\text{DM}} \in [1 \text{ GeV}, 2 \text{ TeV}] \), both for scalar and fermion Dark Matter.

We find that the scalar case is an interesting extension of the Higgs portal. Indeed, in the usual portal the constraints on the Higgs invisible decay and Dark Matter nucleon cross section rule out the possibility of the scalar as the main component of Dark Matter for \( m_{\phi} \lesssim 100 \text{ GeV} \). But in our scenario, annihilation can occur via the neutrino portal which is dominant, i.e. more than 90\%, in most of the parameter space. On the other hand, in the case of a fermion Dark Matter, the contribution to the quark-Dark Matter scattering and Higgs invisible width decay is at one loop and the Higgs portal coupling is only mildly constrained.

Finally we explore the indirect detection characteristics of this model, determined by the decays of the right-handed neutrinos into SM bosons and leptons. We consider constraints from Fermi-LAT and find that those could be sensitive to Dark Matter up to the electroweak scale, \( m_{\text{DM}} \lesssim 100 \text{ GeV} \) independently of whether the Dark Matter particle is a scalar or a fermion. However, a more detailed analysis of these constraints need to be done, as we performed a naive scaling on constraints of Dark Matter decays to two SM particles. In our scenario, the more complex decays of right-handed neutrinos would lead to less energetic SM probes. Finally, we also comment on the possibility of this channel to be responsible of the gamma-ray galactic excess at few GeV.

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Appendix: Sterile neutrino decay widths

Here we summarize the sterile neutrino decay modes, relevant for indirect Dark Matter searches.

If the sterile neutrino is lighter than the W boson, it will decay through off-shell \( h, Z, W \) bosons to three fermions. Since the decay via a virtual \( h \) is further suppressed by the small Yukawa couplings of the SM fermions, it is a good approximation to consider only the processes mediated by virtual \( W, Z \), whose partial widths read [56]:

\[
\Gamma(N \rightarrow \nu_{\ell}q\bar{q}) = 3AC_{NN}[2(a^2_u + b^2_{\nu}) + 3(a^2_\nu + b^2_\nu)]f(z) \quad (A.1)
\]

\[
\Gamma(N \rightarrow 3\nu) = AC_{NN} \left[ \frac{3}{4}f(z) + \frac{1}{4}g(z, z) \right] \quad (A.2)
\]

\[
\Gamma(N \rightarrow \ell q\bar{q}) = 6AC_{NN}f(w, 0) \quad (A.3)
\]

\[
\Gamma(N \rightarrow \nu_{\ell}e\nu) = AC_{NN}[3(a^2_e + b^2_e)]f(z) + 3f(w) - 2a_\nu g(z, w) \quad (A.4)
\]

where \( C_{NN} \) is defined in Eq. (10).

\[
A \equiv \frac{G_F^2 m_N^5}{192 \pi^3} \quad , (A.5)
\]

\( a_f, b_f \) are the left and right neutral current couplings of the fermions \( f = \nu, \ell \), the variables \( z, w \) are given by

\[
z = (m_N/m_Z)^2, \quad w = (m_N/m_W)^2 \quad , (A.6)
\]

and the functions \( f(z), f(w, 0) \) and \( g(z, w) \) can be found in [57].

For larger values of \( m_N \), two-body decays to SM particles are open, and the corresponding widths read [14]:

\[
\Gamma(N \rightarrow W^\pm \ell \nu_\ell) = \frac{g^2}{64\pi}|U_{aN}|^2 m_N^2 \frac{3}{2} \left( 1 - \frac{m_W^2}{m_N^2} \right)^2 \left( 1 + \frac{2m_W^2}{m_N^2} \right) \quad (A.7)
\]

\[
\Gamma(N \rightarrow Z \nu_\ell) = \frac{g^2}{64\pi c_W^2} |C_{aN}|^2 m_N^2 \frac{3}{2} \left( 1 - \frac{m_Z^2}{m_N^2} \right)^2 \left( 1 + \frac{2m_Z^2}{m_N^2} \right) \quad (A.8)
\]
\[ \Gamma(N \rightarrow \ell \nu_{\ell}) = \frac{g^2}{64\pi}[C_{\alpha N}]^2 \frac{m_N^3}{m_W^2} \left( 1 - \frac{m_\ell^2}{m_N^2} \right)^2 \] (A.9)

In the above expressions, we have assumed that \( N\) is a Majorana fermion. If it is Dirac, then the decay channel \( N \rightarrow W^- \ell^+ \) is forbidden and the decay widths into \( Z/\ell, \nu \) are \( \Gamma_D(N \rightarrow Z/\ell \nu) = \Gamma_M(N \rightarrow Z/\ell \nu) / 2 \).

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