Class Adaptive Network Calibration

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Abstract

Recent studies have revealed that, beyond conventional accuracy, calibration should also be considered for training modern deep neural networks. To address miscalibration during learning, some methods have explored different penalty functions as part of the learning objective, alongside a standard classification loss, with a hyper-parameter controlling the relative contribution of each term. Nevertheless, these methods share two major drawbacks: 1) the scalar balancing weight is the same for all classes, hindering the ability to address different intrinsic difficulties or imbalance among classes; and 2) the balancing weight is usually fixed without an adaptive strategy, which may prevent from reaching the best compromise between accuracy and calibration, and requires hyper-parameter search for each application. We propose Class Adaptive Label Smoothing (CALS) for calibrating deep networks, which allows to learn class-wise multipliers during training, yielding a powerful alternative to common label smoothing penalties. Our method builds on a general Augmented Lagrangian approach, a well-established technique in constrained optimization, but we introduce several modifications to tailor it for large-scale, class-adaptive training. Comprehensive evaluation and multiple comparisons on a variety of benchmarks, including standard and long-tailed image classification, semantic segmentation, and text classification, demonstrate the superiority of the proposed method. The code is available at https://github.com/by-liu/CALS.

1. Introduction

Deep Neural Networks (DNNs) have become the prevailing model in machine learning, particularly for computer vision [13] and natural language processing applications [44]. Increasingly powerful architectures [3,13,24], learning methods [4,12] and a large body of other techniques [15,27] are constantly introduced. Nonetheless, recent studies [11,31] have shown that regardless of their superior discriminative performance, high-capacity modern DNNs are poorly calibrated, i.e., failing to produce reliable predictive confidences. Specifically, they tend to yield over-confident predictions, where the probability associated with the predicted class overestimates the actual likelihood. Since this is a critical issue in safety-sensitive applications like autonomous driving or computational medical diagnosis, the problem of DNN calibration has been attracting increasing attention in recent years [11,31,38].

Current calibration methods can be categorized into two main families. The first family involves techniques that perform an additional post-processing parameterized operation on the output logits (or pre-softmax activations) [11], with the calibration parameters of that operation obtained from a validation set by either learning or grid-search. Despite the simplicity and low computational cost, these methods have empirically proven to be highly effective [8,11]. However, their main drawback is that the choice of the optimal calibration parameters is highly sensitive to the trained model instance and validation set [22,31].

The second family of methods attempts to simultaneously optimize for accuracy and calibration during network training. This is achieved by introducing, explicitly or implicitly, a secondary optimization goal involving the model’s predictive uncertainty, alongside the main training objective. As a result, a scalar balancing hyper-parameter is required to tune the relative contribution of each term in the overall loss function. Some examples of this type of approaches include: Explicit Confidence Penalty (ECP) [38], Label Smoothing (LS) [32], Focal Loss (FL) [21] and its variant, Sample-Dependent Focal Loss (FLSD) [31]. It has been recently demonstrated in [22] that all these methods can be formulated as different penalty terms that enforce the same equality constraint on the logits of the DNN: driving the logit distances towards zero. Here, logit distances refers to the vector of L1 distances between the highest logit value and the rest. Observing the non-informative nature of this equality constraint, [22] proposed to use a generalized inequality constraint, only penalizing those logits for which the distance is larger than a pre-defined margin, achieving state-of-the-art calibration performance on many different benchmarks.

Although learning based methods achieve greater calibra-
Figure 1. Many techniques have been proposed for jointly improving accuracy and calibration during training [11,31], but they fail to consider uneven learning scenarios like high class imbalance or long-tail distributions. We show a comparison of the proposed CALS-ALM method and different learning approaches in terms of Calibration Error (ECE) vs Accuracy on the (a) ImageNet and (b) ImageNet-L T (long-tailed ImageNet) datasets. A lower ECE indicates better calibration: a better model should attain high ACC and low ECE. Among all the considered methods, CALS-ALM shows superior performance when considering both discriminative power and well-balanced probabilistic predictions, achieving best accuracy and calibration on ImageNet, and best calibration and second best accuracy on ImageNet-L T.

Figure 1 shows a comparison of the proposed CALS-ALM method and different learning approaches in terms of Calibration Error (ECE) vs Accuracy on the (a) ImageNet and (b) ImageNet-L T (long-tailed ImageNet) datasets. A lower ECE indicates better calibration: a better model should attain high ACC and low ECE. Among all the considered methods, CALS-ALM shows superior performance when considering both discriminative power and well-balanced probabilistic predictions, achieving best accuracy and calibration on ImageNet, and best calibration and second best accuracy on ImageNet-L T.

2. Related Work

2.1. Problem Formulation

Given a dataset $D = \{(x^{(i)}, y^{(i)})\}_{i=1}^N$ with $N \in \mathbb{N}$ pairs of samples $x \in \mathcal{X}$ and corresponding labels $y \in \mathcal{Y}$, with $\mathcal{Y} = \{1, \ldots, K\}$, a deep neural network (DNN) $F_{\theta} : \mathcal{X} \rightarrow \mathbb{R}^K$ parameterized by $\theta$ yields logits $l = F_{\theta}(x) = (F_{\theta}(x)_k)_{1 \leq k \leq K} \in \mathbb{R}^K$. In a classification scenario, the output probability $s = (s_k)_{1 \leq k \leq K} \in \Delta^{K-1}$, where $\Delta^{K-1} \subset [0,1]^K$ denotes the probability simplex, is
obtained by applying the $\text{softmax}$ function on the output logits, i.e. $s = \text{softmax}(l) = \frac{\exp l}{\sum \exp l}$. Therefore, the predicted class $\hat{y}$ is computed as $\hat{y} = \arg \max_k s_k$, and the predicted confidence is $\hat{p} = s_{\hat{y}} = \max_k s_k$. A perfectly calibrated model should satisfy that the predicted confidence of any input is equal to the accuracy of the model: $\hat{p} = \mathbb{P}(\hat{y} = y | \hat{p})$. Hence, an over-confident model yields on average larger confidences than the associated accuracy, whereas an under-confident model yields lower confidence than its accuracy.

A number of recent studies [11, 22, 30, 31] have shown that DNNs tend to become over-confident during training as a result of minimizing the popular cross-entropy (CE) training loss:

$$L_{\text{CE}}(x, y) = -\sum_{k=1}^{K} y_k \log s_k$$

where $y \in \{0, 1\}^K$ is the one-hot encoding of $y$. This objective function is minimized when the predictions for all the training samples fully match the ground-truth labels $y$, i.e. $s_y = 1$ and $\forall k \neq y, s_k = 0$. The negative logarithmic term on the logit of the correct category renders the global minimization of the CE loss unreachable, as it keeps pushing the predicted probabilities $s$ towards the vertices of the $(K-1)$-simplex even after the classification error is zero [31], resulting in over-confident models.

2.2. Post-processing methods

To address mis-calibration, different post-processing techniques applied after model training have been proposed recently [8, 11, 43]. The most popular of these strategies is Temperature Scaling (TS) [11], which applies a single scalar calibration during training by introducing an additional constraint measure based on RKHS kernels, while [16] proposed a differential calibration loss based on a soft version of the binning operation in the ECE metric. In [5], two types of binary pairwise calibration constraints were proposed as additional penalty terms during training. Other methods try to decrease over-fitting on the cross-entropy loss, which has been demonstrated to be the main reason of over-confidence [11, 31]. In [38] an explicit confidence penalty (ECP) is proposed to maximize the entropy and reduce over-fitting, while Label Smoothing [42] has also been shown to implicitly improve the calibration [32] by softening the hard one-hot targets in the cross-entropy. The Focal Loss [21], originally proposed to tackle class imbalance, can also be effective for calibration [31], as it implicitly minimizes the Kullback-Leibler (KL) divergence between the uniform distribution and the network softmax probabilities, thereby increasing the entropy of the predictions. As an extension the Sample-Dependent Focal Loss (FLSD) was also proposed in [31] to further boost calibration performance.

Margin-based Label Smoothing (MbLS). A unifying constrained-optimization formulation of loss functions promoting calibration has been recently presented in [22]. Specifically, the additional penalties integrated in these methods, including ECP [38], LS [32] and FL [31], can be viewed as different forms of approximations to the same constraint, i.e. enforcing the logit distances to be zero. Noticing that this constraint is non-informative (its solution being uniformly distributed probabilities), [22] further proposed a generalized formulation by relaxing the constraint to allow the logit distances being lower than a strictly positive margin.

The specific formulation of MbLS [22] is as follows. Given a margin $m \in \mathbb{R}_+$, the constrained optimization problem for network training is:

$$\min_{\theta} \sum_{i=1}^{N} L_{\text{CE}}(x^{(i)}, y^{(i)})$$

s.t. \hspace{3mm} $\max_k \{l_k^{(i)}\} - l_j^{(i)} \leq m, \quad i = 1, \ldots, N,$

where $l^{(i)} = F_{\theta}(x^{(i)})$. The minimum can be approximated by penalty-based optimization methods, transforming the above formulation into an unconstrained problem by means of simple ReLU functions:

$$\min_{\theta} \sum_{i=1}^{N} L_{\text{CE}}(x^{(i)}, y^{(i)}) + \lambda \sum_{i=1}^{N} \sum_{j=1}^{K} \max \{0, \max_k \{l_k^{(i)}\} - l_j^{(i)} - m\},$$

where $\lambda \in \mathbb{R}_+$ is a scalar weight balancing contributions of the CE loss and the corresponding penalty.
3. Sample-wise Constrained DNN Optimization

Although MbLS can significantly improve calibration, the associated constrained problem (2) is not solved accurately. It is approximated by an unconstrained problem with a single uniform penalty, regardless of the data sample or category. However, the samples and classes considered in a classification problem have different intrinsic learning difficulties. Therefore, an improved training scheme would involve considering distinct penalty weights \( \lambda \) for each sample and class. This would result in having chosen \( N \times K \) penalty weights \( \Lambda \in \mathbb{R}^{N \times K} \), with the resulting optimization problem being:

\[
\min_{\theta} \sum_{i=1}^{N} \mathcal{L}_{CE}(x^{(i)}, y^{(i)}) + \sum_{j=1}^{K} \sum_{i=1}^{N} \lambda_{ij} \max\{0, \max_{k} l_{k}^{ij} - l_{j}^{ij} - m\}. \tag{4}
\]

From an optimization perspective, supposing that optimal weights \( \theta^{*} \) exists for problem (2), there exists \( \Lambda^{*} \in \mathbb{R}^{N \times K} \) such that \((\theta^{*}, \Lambda^{*})\) is a saddle point of the Lagrangian associated to (2). These \( \Lambda^{*} \) are the Lagrange multipliers of the problem. Therefore, using \( \Lambda = \Lambda^{*} \) would be the best choice to solve (4).

In practice, using the Lagrange multipliers of problem (2) as the weights for the penalties may not be computationally feasible, and it could even result in degraded performance. Indeed, in the context of machine learning, we optimize a model’s weights \( \theta \) to solve (2) on a training set \( D_{\text{train}} \), and expect to generalize on a test set \( D_{\text{test}} \), which we do not have access to during training. Because of the bias-variance trade-off, solving (2) optimally would likely result in overfitting, i.e., we may solve problem (2) accurately on the train set, but not generalize properly on the test set, resulting in poor calibration and classification performance overall. This suggests that it could be preferable to evaluate during training the quality of multipliers on a separate validation set \( D_{\text{val}} \). Additionally, several mechanisms for training DNNs are not compatible with a straightforward minimization. First, the use of batch normalization yields predictions that are not independent between samples in a minibatch. Second, the use of regularization techniques such as dropout may lead to virtually inaccurate predictions on certain training samples, impacting the correct estimation of multipliers. Third, data augmentation, which is standard in DNN training, would result in additional penalty weights for the augmented samples: they can be easier or harder to classify than the original ones.

In addition to the above obstacles, applying a penalty weight per sample and per class (resulting in \( N \times K \) weights) would not scale well for large datasets and dense predictive tasks, such as semantic segmentation, which is typically formulated as a per-pixel classification task. Assuming that images in the dataset have a size of \( H \times W \), this would result in \( N \times H \times W \times K \) penalty weights. This rapidly becomes a limiting factor for moderately sized segmentation datasets. For instance, Pascal VOC 2012 \[9\] contains 21 classes and 1464 training images, amounting to \( 2.62 \times 10^8 \) pixels, or \( 5.5 \times 10^9 \) penalty weights, which, stored as float32, would use \(~20\) GiB. For Cityscapes [6], containing approximately 3000 training images of size \( 2048 \times 1024 \) in 19 classes, this amounts to \(~445\) GiB.

Following the above observations, we introduce a relaxation of sample-wise penalties, and propose to solve the following problem:

\[
\min_{\theta} \sum_{i=1}^{N} \mathcal{L}_{CE}(x^{(i)}, y^{(i)}) + \sum_{j=1}^{K} \sum_{i=1}^{N} \lambda_{ij} \max\{0, \max_{k} l_{k}^{ij} - l_{j}^{ij} - m\}, \tag{5}
\]

where \((\lambda_{ij})_{1 \leq j \leq K} \in \mathbb{R}^{K}\). Since penalties are now class-wise, we need \( K \) penalty weights. This has the advantage to scale well to denser classification tasks such as segmentation. However, we still face a challenging optimization problem (5), since we still need to chose \( K \) weights, which can be extremely complicated for large-scale datasets with many classes such as ImageNet, which contains 1000 classes. In the next section, we introduce a numerical technique to deal with this challenge.

4. Class Adaptive Network Calibration

The challenge of the previous formulation stems from correctly choosing the weights \( \Lambda \in \mathbb{R}^{K} \), which can be cumbersome when \( K \) is large. Therefore, we propose to use an Augmented Lagrangian Multiplier (ALM) method to adaptively learn the weights of the penalties.

4.1. General ALM

ALM methods combine penalties and primal-dual updates to solve a constrained problem. They have well-established advantages and enjoy widespread popularity in the general context of optimization [1, 35, 41]. Specifically, we have the following generic constrained optimization problem:

\[
\min_{x} f(x) \quad \text{s.t.} \quad h_{i}(x) \leq 0, \quad i = 1, \ldots, n \tag{6}
\]

where \( f : \mathbb{R}^{d} \rightarrow \mathbb{R} \) is the objective function and \( h_{i} : \mathbb{R}^{d} \rightarrow \mathbb{R}, i = 1, \ldots, n \) are the constraint functions. We tackle it by approximately solving a sequence \( j \in \mathbb{N} \) of unconstrained problems:

\[
\min_{x} \mathcal{L}^{(j)}(x) = f(x) + \sum_{i=1}^{n} P(h_{i}(x), \rho_{i}^{(j)}, \lambda_{i}^{(j)}) \tag{7}
\]
with $P : \mathbb{R} \times \mathbb{R}^n_+ \times \mathbb{R}^n_+ \to \mathbb{R}$ a penalty-Lagrangian function, and $\rho^{(j)} = (\rho_i)_{1 \leq i \leq n} \in \mathbb{R}^n_+$, $\lambda^{(j)} = (\lambda_i^{(j)})_{1 \leq i \leq n} \in \mathbb{R}^n_+$ the penalty parameters and multipliers associated to $P$ at the $j$-th iteration. This sequence of unconstrained problems is called outer iterations, while the steps in the minimization of $\mathcal{L}^{(j)}$ are called inner iterations.

The main components of ALM methods are (i) the penalty-Lagrangian function $P$, (ii) the update of the penalty multipliers $\lambda^{(j)}$ and (iii) the increase of the penalty parameters $\rho^{(j)}$. First, the penalty function $P$ needs to satisfy a set of axioms [2] (see Appendix A): these axioms constrain the function to be continuously differentiable w.r.t. its first variable and to have a non-negative derivative: $\forall z \in \mathbb{R}, P'(z, \rho, \lambda) = \frac{\partial}{\partial z} P(z, \rho, \lambda) \geq 0$, with $P'(0, \rho, \lambda) = \lambda$. Figure 2 gives an example of a penalty, and how $\rho$ and $\lambda$ affect it. The choice of penalty function is critical to the performance of ALM methods, especially for nonconvex problems [2]. Typical functions include PHR [14,39], $P_2$ [17] and $P_3$ [34] (see section 3.2 of [2]). Second, the penalty multipliers $\lambda^{(j)}$ are updated to the derivative of $P$ w.r.t. the solution obtained during the last inner minimization. Formally, let $x^{(j)}$ be the approximate minimizer of $\mathcal{L}^{(j)}$, then $\forall i \in \{1, \ldots, n\}$:

$$\lambda^{(j+1)}_i = P'(h_i(x^{(j)}), \rho^{(j)}_i, \lambda^{(j)}_i)$$

This update rule corresponds to a first-order multiplier estimate for the constrained problem. Third, the penalty parameters $\rho^{(j)}$ are increased during the outer iterations if the constraints do not improve (i.e. is closer to being satisfied) compared to the previous outer iteration. Typically, $\rho^{(j+1)}_i = \gamma \rho^{(j)}_i$ if $h_i$ does not improve, with $\gamma > 1$.

When the problem is convex, alternating between the approximate minimization of (7) and the update of the multipliers (8) leads to a solution for the constrained problem. The inner minimization corresponds to minimizing the primal while the outer iterations correspond to solving the dual problem. The complete procedure is presented in Algorithm 1.

Although guarantees exist only in the convex case, it is well-known that ALM methods can efficiently solve nonconvex problems as well [2]. In the context of deep learning, their use has been surprisingly underexplored [40,41].

**Algorithm 1 Augmented Lagrangian Multiplier algorithm**

**Require:** Objective function $f$

**Require:** Constraint functions $h_i, i = 1, \ldots, n$

**Require:** Penalty function $P$, initial $\lambda^{(0)} \in \mathbb{R}^n_+$, $\rho^{(0)} \in \mathbb{R}^n_+$

**Require:** Initial variable $x^{(0)}$, iterations $j = 1$

1: while not converged do
2: Initialize with $x^{(j-1)}$ and minimize (approximately):
3: $\mathcal{L}^{(j)}(x) = f(x) + \sum_{i=1}^n P(h_i(x), \rho_i^{(j)}, \lambda_i^{(j)})$
4: $x^{(j)} \leftarrow$ (approximate) minimizer of $\mathcal{L}^{(j)}$
5: for $i = 1, \ldots, n$ do
6: $\lambda_i^{(j+1)} \leftarrow \gamma \rho_i^{(j)}$
7: else
8: $\rho_i^{(j+1)} \leftarrow \rho_i^{(j)}$
9: end if
10: end for
11: $j \leftarrow j + 1$
12: end while

**4.2. ALM for calibration**

Our goal now is to build an ALM method effective for calibration purposes. We can achieve this by reformulating problem (5) using a penalty function $P$ parameterized by $(\rho, \lambda) \in \mathbb{R}^n_+ \times \mathbb{R}^n_+$ as follows:

$$\min_\theta \sum_{i=1}^N \mathcal{L}_{CE}(x^{(i)}, y^{(i)}) + \sum_{k=1}^K P(d_k^{(i)} - m, \rho_k, \lambda_k)$$

where $d_k^{(i)} = \max\{0, l_k^{(i)} - t_k^{(i)}\} \in \mathbb{R}_+$. With this formulation, it is natural to use a penalty-Lagrangian function for $P$. To avoid numerical issues typically associated with non-linear penalties, we normalize the constraints by the margin $m > 0$:

$$d_k^{(i)} - m \leq 0 \iff \frac{d_k^{(i)}}{m} - 1 \leq 0$$

This leads to improved numerical stability for the ALM multiplier update as well. Additionally, we average the constraints instead of summing them. This makes the method independent of the number of classes, and eases the choice of initial penalty parameters $\rho^{(0)}$. The resulting loss is:

$$\sum_{i=1}^N \mathcal{L}_{CE}(x^{(i)}, y^{(i)}) + \frac{1}{K} \sum_{k=1}^K P\left(\frac{d_k^{(i)}}{m} - 1, \rho_k, \lambda_k\right)$$

As noted in Section 3, one of the main downsides of estimating Lagrange multipliers from the training set is that...
we could quickly overfit the data. Therefore, we propose to use the validation set to obtain a reliable estimate of the penalty multipliers at each epoch. We consider that an epoch of training corresponds to the approximate minimization of the loss function, and then compute the average penalty multiplier on the validation set. Formally after a training epoch \( j \), the penalty multipliers for epoch \( j+1 \) will be, for all \( k = 1, \ldots, K \):

\[
\lambda^{(j+1)}_k = \frac{1}{|\mathcal{D}_{val}|} \sum_{(x, y) \in \mathcal{D}_{val}} P'(\frac{d_k}{m} - 1, \rho_k^{(j)}, \lambda_k^{(j)})
\]

(12)

Finally, the penalty multiplier is projected on a safeguarding interval \([\lambda_{\min}, \lambda_{\max}] = [10^{-6}, 10^{6}]\) in our case. To update the penalty parameters \( \rho \), we compute the average constraint per class on the validation set. Then, for each class, if the average constraint is positive and has not decreased compared to the previous epoch, we multiply the corresponding penalty parameter by \( \gamma \).

Finally, as suggested by \[2\] and confirmed by our empirical results, we utilize the PHR function in our implementation, defined as follows:

\[
\text{PHR}(z, \rho, \lambda) = \begin{cases} 
\lambda z + \frac{1}{2} \rho z^2 & \text{if } \lambda + \rho z \geq 0; \\
\frac{\lambda^2}{2\rho} & \text{otherwise.}
\end{cases}
\]

(13)

Overall, the proposed method, consolidated in Algorithm 2, corresponds to approximately solving the constrained problem (2), by learning class-wise penalty multipliers on the validation set, to avoid overfitting and training specificities (i.e., batch normalization, dropout, augmentations) which would result in unreliable penalty multipliers estimates.

5. Experiments

5.1. Experimental Setup

Datasets. We perform experiments on a variety of popular benchmarks. First, we include three widely used image classification benchmarks, including Tiny-ImageNet \[7\], ImageNet \[7\] and one long-tailed image classification, ImageNet-LT \[25\]. Tiny-ImageNet is widely used in the calibration literature \[22, 31\], with relatively small \( 64 \times 64 \) resolution, while ImageNet \[7\] is a large-scale benchmark consisting of 1000 categories and over 1M images. The main characteristic of ImageNet-LT is that the number of samples is extremely imbalanced across classes, ranging from 5 to 1280. To evaluate performance in dense prediction tasks, we include one semantic segmentation benchmark, PASCAL VOC2012 \[9\]. Furthermore, one benchmark from the NLP domain, 20NewsGroups \[19\], is included to show the general applicability. For a detailed description of each dataset and the pre-processing settings, please refer to Appendix B.

Evaluation Metrics. For calibration, we report the most widely used Expected Calibration Error (ECE) \[33\]. Samples are grouped into \( M \) equi-spaced bins according to prediction confidence, and a weighted average of the absolute difference between accuracy and confidence in each bin is calculated:

\[
ECE = \sum_{m=1}^{M} \frac{|B_m|}{N} |A_m - C_m|, 
\]

(14)

where \( M \) is the number of bins, \( N \) the amount of test samples, \( B_m \) the samples with prediction confidence in the \( m^{th} \) bin, \( A_m \) the accuracy and \( C_m \) the mean confidence of samples in the \( m^{th} \) bin. Note we fix \( N \) to 15 according to \[22, 31\]. In accordance with \[22\], we also report Adaptive ECE (AECE), a variant of ECE where the bins are configured to evenly distribute the test samples across them. Additionally, Classwise Calibration Error (CWCE) \[29\], a classwise extension of ECE, is included in Appendix C. For discriminative performance, we use standard measures: accuracy (Acc) for classification, and intersection over union (mIoU) for segmentation.

Compared methods. We compare our method to other learning based calibration losses, including (i) methods that impose constraints on predictions (either logits or softmax probabilities), i.e. Explicit Confidence Penalty (ECP) \[38\], Label Smoothing (LS) \[42\], Focal Loss (FL) \[21\] and its sample-dependent version (FLSD) \[31\], Margin-based Label
We refer to the related literature [22,31] to set the margin to $\mu > 1$ where $\mu$ is a hyper-parameter for various methods. For instance, the smoothing factor in LS and FL is set to 0.05 and 3 respectively, and we set margin to 10 in MbLS. A detailed description of hyper-parameter values can be found in Appendix F.

**Our methods.** A simple alternative to the algorithm presented in Section 4.2 would be to heuristically tune multipliers by scaling them according to penalty values: if $P^{(j+1)}_{k,j}$ increases we also increase $\lambda^{(j+1)}_{k,j}$ and vice versa. This strategy, akin to learning rate scheduling, can be formulated as:

$$
\lambda^{(j+1)}_{k,j} = \begin{cases}
\mu \lambda_{k,j}^{(j)} & \text{if } P^{(j+1)}_{k,j} > \tau P^{(j)}_{k,j} \\
\lambda_{k,j}^{(j)} / \mu & \text{if } P^{(j+1)}_{k,j} > \tau P^{(j+1)}_{k,j} \\
\lambda_{k,j}^{(j)} & \text{otherwise}
\end{cases}
$$

where $\mu > 1$ and $\tau > 1$ are hyper-parameters that we fix to 1.1. We refer to our main algorithm as CALS-ALM and to this heuristic rule as CALS-HR in what follows.

We fix the margin to $m = 10$ on vision tasks and $m = 6$ on the NLP benchmark, as in [22], for a fair comparison. We also perform an ablation study to investigate the impact of the margin value. For other hyper-parameters, we set $\lambda^{(0)} = 10^{-6}$, $1_K$, $\rho^{(0)} = 1_K$, $\gamma = 1.2$, and we update the penalty parameters $\rho$ every 10 epochs. Please refer to Appendix F for a detailed description of all hyper-parameters.

**Implementation Details.** For image classification, we experiment with ResNet [13] and a vision Transformer model, i.e., Swin Transformer V2 (SwinV2-T) [23]. DeepLabV3 [3] is employed for semantic segmentation on PASCAL VOC2012. Following [22,31], we use the Global Pooling CNN (GPoC-CNN) architecture [20] on the NLP recognition task. Further training details on each dataset can be found in Appendix B.

### 5.2. Results

**Results on image classification.** Table 1 presents the discriminative and calibration performance of our methods across three widely used classification benchmarks, compared to baselines and related works. We can observe that our CALS-ALM approach consistently outperforms existing techniques in terms of calibration. Specifically, the results indicate that the standard CE loss and other approaches often lead to miscalibrated models, with the severity of miscalibration substantially increasing in correlation with dataset difficulty. This is particularly evident in large-scaled datasets with numerous classes, such as ImageNet, or those with long-tail class distributions, like ImageNet-LT. Although other learning-based methods could provide better calibrated networks, their performance is not stable across different settings. For example, while FL achieves a relatively low ECE of 1.60 with a ResNet50 trained on ImageNet, it only yields an ECE of 25.50 when training a SwinV2-T network on ImageNet-LT, revealing a limitation in adapting to different learning scenarios. In contrast, CALS-ALM attains the best calibration performance in all cases, frequently outperforming existing approaches by a significant margin, with minimal variations across datasets and architectures.

In terms of model accuracy, our method delivers competitive performances, surpassing existing methods in certain cases. It is important to emphasize that, while the proposed method achieves discriminative results comparable to the best-performing approach for each dataset, the differences in calibration are considerable. This highlights the superiority of the proposed formulation for training highly discrимi-

| Method       | TinyImageNet | ImageNet | ImageNet-L T |
|--------------|--------------|----------|--------------|
|               | ResNet-50    | ResNet-50 | SwinV2-T     |
| CE           | 65.02        | 75.16    | 57.58        |
| MMCE [18]    | 64.34        | 74.85    | 56.70        |
| ECP [38]     | 64.90        | 75.22    | 58.12        |
| LS [42]      | 65.78        | 76.04    | 55.98        |
| FL [31]      | 63.09        | 73.87    | 53.56        |
| FLSD [31]    | 64.09        | 73.97    | 54.70        |
| CPC [5]      | 64.49        | 73.36    | 56.34        |
| MbLS [22]    | 64.74        | 75.82    | 55.74        |
| CALS-HR      | 65.09        | 76.34    | 57.58        |
| CALS-ALM     | 65.03        | 76.44    | 57.30        |

Table 1. Calibration performance for different approaches on three image classification benchmarks. We report two lower-is-better calibration metrics, i.e, ECE and AECE. Best method is highlighted in bold, while the second-best one is underlined.
native and well-calibrated networks. Figure 1 provides a more visual comparison considering both accuracy and ECE. It is demonstrated that CALS-ALM provides the optimal compromise between accuracy and calibration performance.

Ablation Analysis. Figure 3 illustrates the evolution of ECE in (a) and penalty multipliers $\lambda$ in (b) during training. It is interesting to observe that the evolution of $\lambda$ is consistent with the ECE. Specifically, the average penalty weight gradually increases while the ECE initially deteriorates because the model is focused on increasing accuracy. However, the value of the penalty weight begins to decline alongside the ECE, as the network starts to become better calibrated. For a visualization of classwise multipliers, please refer to Appendix D. Figure 3(c) highlights the impact of the choice of penalty functions and margin values. This demonstrates that the PHR penalty function is preferable over the other two options, P2 and P3, for both calibration and accuracy. Regarding the margin, the best performance is achieved with $m \approx 10$, which is consistent with the findings in [22].

Semantic Segmentation. Table 2 presents the performance on Pascal VOC dataset. Note here CALS refers to our best method, i.e. CALS-ALM. It can be observed that the trend is consistent with image classification experiments: CALS outperforms counterparts in terms of ECE, and yields competitive results on discriminative performance, i.e. mIoU in segmentation. It is worth noting that some methods like MMCE, FLSD and CPC, are not included here because their computation demands were too heavy for pixel-wise segmentation tasks. In contrast, our method is unlimited in dense prediction tasks as the computation cost it adds is moderate.

Text Classification. Last, we demonstrate the general applicability of the proposed method by analyzing its performance on a non-vision task, i.e. text classification on 20 Newsgroups dataset. The results are reported in Table 3. Remarkably, CALS again brings substantial improvement in terms of calibration, with ECE decreasing to 2.04\%, while yielding the best accuracy 68.32\%. This reveals that the proposed class adaptive learning method is also able to handle class differences in NLP applications and provide promising performance in terms of both accuracy and calibration.

6. Limitations and Future Work

We have proposed Class Adaptive Label Smoothing for network calibration based on a modified Augmented Lagrangian Multiplier algorithm. Despite its superior performance over previous methods, there are potential limitations in this work. For instance, our method requires the validation set to have the same distribution as the training set. Although this is satisfied in nearly every benchmark, it will be interesting to investigate the impact of using non-independent and identically distributed (i.i.d) validation sets.

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