Thermal-induced proteinquake in oxyhemoglobin

S. G. Gevorkian\textsuperscript{1,3}, A.E. Allahverdyan\textsuperscript{2,3}, D.S. Gevorgyan\textsuperscript{4}, Chin-Kun Hu\textsuperscript{1}\textsuperscript{*}

\textsuperscript{1}Institute of Physics, Academia Sinica, Nankang, Taipei 11529, Taiwan
\textsuperscript{2}Laboratoire de Physique Statistique et Systèmes Complexes, ISMANS, 44 ave. Bartholdi, 72000 Le Mans, France
\textsuperscript{3}Yerevan Physics Institute, Alikhanian Brothers St. 2, Yerevan 375036, Armenia and
\textsuperscript{4}Institute of Fine Organic Chemistry, 26 Azatutian ave., Yerevan 0014, Armenia

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Oxygen is released to living tissues via conformational changes of hemoglobin from R-state (oxyhemoglobin) to T-state (desoxyhemoglobin). The detailed mechanism of this process is not yet fully understood. We have carried out micromechanical experiments on oxyhemoglobin crystals to determine the behavior of the Young’s modulus and the internal friction for temperatures between 20 C and 70 C. We have found that around 49 C oxyhemoglobin crystal samples undergo a sudden and strong increase of their Young’s modulus, accompanied by a sudden decrease of the internal friction. This sudden mechanical change (proteinquake) takes place in a partially unfolded state and precedes the full denaturation transition at higher temperatures. The hemoglobin crystals after the proteinquake has the same mechanical properties as the initial state at room temperatures. We conjecture that it can be relevant for explaining the oxygen-releasing function of native oxyhemoglobin when the temperature is increased, e.g. due to active sport. The effect is specific for the quaternary structure of hemoglobin, and is absent for myoglobin with only one peptide sequence.

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Since its discovery in 1840, the hemoglobin is one of the most extensively studied proteins\textsuperscript{1,2}. This is related to its important physiological function: it carries oxygen from the lungs throughout the body allowing us to breathe and live. It consists of four globular units linked into a double-dimer tetrameric structure\textsuperscript{1,2} as shown schematically in Fig. 1. Each unit can carry one oxygen molecule O\textsubscript{2} attached to its heme group. The hemoglobin structure is adapted to the needs of its function. First, its oxygen binding is cooperative: the response of hemoglobin with respect to O\textsubscript{2} concentration has a S-shaped region, thereby a relatively slight decrease of the oxygen concentration between the lungs and the body brings in a significant decrease of the bound oxygen (up to 25%)\textsuperscript{1,2}. Second, the oxygen binding ability decreases upon reducing the pH factor or increasing the concentration of CO\textsubscript{2}\textsuperscript{3}. Due to this Bohr’s effect\textsuperscript{3} a tissue with a stronger need of oxygen receives it more. Cooperative oxygen unbinding of hemoglobin is explained by the change of its tetrameric conformational structure induced by binding of the first oxygen molecule\textsuperscript{2}; see Fig. 1. The conformational states with (R-state or oxyhemoglobin) and without (T-state or desoxyhemoglobin) the four oxygen molecules are clearly distinguishable by their shape, as seen via X-ray crystallography\textsuperscript{1,2}. In vivo those states are more like dynamic ensembles than fixed conformations\textsuperscript{4}.

Many aspects of hemoglobin are well understood by now\textsuperscript{2}. However, the physics of conformational changes and their interaction with external factors (pressure, oxygen concentration, temperature) is still under active scrutiny\textsuperscript{5,6}. In particular, this concerns the thermal response of hemoglobin that is traditionally studied via denaturation experiments. It is known that the multidomain hemoglobin does not unfold via a single transition\textsuperscript{5}. Rather, there is a wide transition zone $\simeq 40^\circ - 60^\circ$ C that includes several events\textsuperscript{6}. These events are typically interpreted via the concepts of unfolding and/or internal aggregation, two standard mechanisms normally applied for describing thermal responses of multi-subunit proteins\textsuperscript{6,7}.

Here we report results of micromechanical experiments carried out on crystals of horse and human hemoglobin. We show that in its partially unfolded state—i.e. for a temperature higher than the physiological temperatures, but lower than the unfolding temperature—the hemoglobin responds to heating by a sudden release of force and a subsequent jump of the Young’s modulus, which is similar to proteinquake reported by Ansari et al.\textsuperscript{6}. The detailed structure of this effect is different for human and horse hemoglobin. We argue that the effect relates to certain slowly relaxing degrees of freedom of the quaternary structure that accumulate energy during heating and then suddenly release it at a well-defined temperature that is specific for hemoglobin.

Such an effect is absent in the thermal response of myoglobin. This is a single-unit globular protein that displays a visible transition towards a partially denaturated state around a certain unfolding temperature\textsuperscript{6}. Myoglobin also

* E-mail: huck@phys.sinica.edu.tw.
binds and unbinds oxygen, but does so without a sizable cooperativity. This relates to its function: myoglobin is a depot (not transporter) of oxygen in muscles. The difference between hemoglobin and myoglobin was also observed in heating and re-cooling data of Young’s modulus for two systems to be reported below.

The proteinquake reported here for hemoglobin crystals has several predecessors in biopolymer physics. Ansari et al. found an indirect experimental evidence that the low-temperature ligand unbinding of myoglobin is modulated by a sudden release of energy accumulated due to the ligand binding \[9\]. They proposed the term *proteinquake* for such effects. Later on, it was found computationally that proteinquakes are relevant for the functioning of myosin \[10\] and adenylate kinase \[11\]. More specifically for hemoglobin, it is known that when crystals of deoxyhemoglobin are exposed to oxygen, they shatter due to the force released during the conformational transition from deoxy to oxyhemoglobin \[12\] \[13\]. Postponing detailed connections with literature till the end of this paper, we stress already here that the presented report seems to be the first one, where a proteinquake effect was found under heating which is generally supposed to diminish mechanical features of biopolymers.

Note in this context that the advantage of using biopolymer crystals for measurement is that there is a possibility of controlling and displaying—via intermolecular contacts regulated by the crystal syngony and the water content—those motions of the macromolecule that can have only transient character in the solution \[14\] \[15\]. Almost all the basic information on the hemoglobin structure came from experiments on solid-state hemoglobins. Figure 2 illustrates the structure of the hemoglobin crystal \[1\] \[2\] \[16\] \[17\]. The solid state hemoglobin is closer to its in vivo state in mammal erythrocytes, where the hemoglobin is densely packed with concentration \(\simeq 34\%\) \[18\].

**Results**

1. We start with the denaturation curve of the human oxyhemoglobin at relative humidity 95% as shown in Fig. 3. The Young’s modulus \(E\) is stable between 25°C and 36°C and then decreases in discrete steps. In between of each step \(E\) is constant. We argue below that that these discrete steps are related to partial dissociation of the quaternary structure. The measured internal friction \(\theta\) increases, because the structure breaking liberates new degrees of freedom that are able to dissipate the energy of forced oscillations; see Fig. 4.

   But we could not perform the experiment for temperatures higher than 49°C, because (at the employed excitation frequency \(\simeq 5\) kHz of the plate oscillations) the crystals close to pieces. The measurement of \(\theta\) had to be terminated even earlier due to instability of results; see Fig. 3. The same breaking effect at 49°C was observed for crystals of horse hemoglobin prepared under the same relative humidity 95%. This effect indicates on conformational changes taking place in the hemoglobin macromolecule. Recall in this context that deoxyhemoglobin crystals shatter after exposure to oxygen, since they cannot support a large conformational change related to the transition from deoxy to oxyhemoglobin \[12\] \[13\]. The difference with our situation is that we work with oxyhemoglobin and that with us the crystals shatter after heating.

2. To understand this effect, we equilibrated our samples under a smaller relative humidity of 75% at 25°C. This was expected to prevent strong instabilities in the crystal \[19\], since inter-molecular contacts in the crystal get stronger due to less inter-molecular water (Fig. 2). Figure 4 displays the behavior of the Young’s modulus for the human and horse hemoglobin under heating at relative humidity 75%. Note that compared to the 95%-humidity, the absolute value of the Young’s modulus increased for about 8 times; cf Fig. 4 with Fig. 8.

   For temperatures from 20°C till 49°C the Young’s modulus \(E\) of the human hemoglobin decreases again in discrete steps. However, due to less inter-molecular water these steps are now shorter. Indeed, consider the temperature interval 25°C–36°C. For 95%-humidity \(E\) is constant there [see Fig. 3], but for 75%-humidity it still makes one sudden change in this interval; see Fig. 4. Hence the inter-molecular water does stabilize the hemoglobin structure against dissociation, though it decreases the absolute value of \(E\). For horse hemoglobin the decay of \(E\) for temperatures from 20°C till 49°C is more gradual, but the stepwise change is still visible; see Fig. 4.

3. But the temperature 49°C is again a special one both for the human and horse hemoglobin; see Figs. 4, 5, and 6 In its vicinity, the Young’s modulus \(E\) changes abruptly. We prescribe these effects to the quaternary structure of hemoglobin, since myoglobin which lacks this structure, but still has well-defined tertiary and secondary structure does not show this effect [see Fig. 7 and Fig. 8 below]. Thus, it is plausible that certain degrees of freedom of the quaternary structure have long relaxation times. During gradual heating, they go out of equilibrium, accumulate energy in elastic deformations and then suddenly release this strain energy at 49°C (proteinquake).

   The abrupt change of the Young’s modulus for relative humidity 75% is clearly the same effect that is responsible for breaking the crystals at a larger relative humidity 95%, where inter-molecular contacts are weaker [see 1]. However, for the human hemoglobin \(E\) abruptly decreases at 49°C, while for the horse hemoglobin it abruptly increases. We see that the precise type of the mechanical event—i.e., whether its Young’s modulus increases or decreases—depends on the type of hemoglobin (human or horse), but the temperature of the event is to a larger extent independent of the type, as Fig. 4 shows [we come back to this difference in 4]. It is also independent from the relative humidity, in
contrast to the absolute value of \( E \) and the pattern of its change.

Figure 6 presents the behavior of both \( \theta \) and \( E \) for the horse hemoglobin. It is seen that in the immediate vicinity of 49°C, \( \theta \) abruptly decreases basically to the value it had at \( \simeq 35^\circ C \). This indicates that the degrees of freedom liberated during the previous melting stage get blocked again.

The evolution of \( E \) and \( \theta \) under heating with temperatures higher than 50°C is different: \( \theta \) starts to grow again indicating a new trend in structure breaking; see Fig. 6. But \( E \) gradually increases for both human and horse hemoglobin; see Fig. 4. We interpret this effect via the intra-tetrameric aggregation of partially denaturated monomers of hemoglobin, because such increase of \( E \) is absent for the monomeric myoglobin; see Fig. 4 below.

It is impossible to prescribe the event at 49°C to the aggregation only, because the changes of \( E \) and \( \theta \) take place within a too narrow temperature interval. We also cannot prescribe this effect to unfolding, since the decreasing \( \theta \) indicates on ordering (rather than disordering) of certain degrees of freedom. Apparently, the only possibility left is that the event at 49°C indicates on the transition of the partially denaturated tetramer from the R-state to another conformational state with different visco-elastic features.

Figure 6 displays the heating-recooling dynamics of the human hemoglobin at relative humidity 95% around 49°C. The effect is irreversible, but the initial value of \( E \) is roughly recovered for 30°C, albeit the characteristic stepwise pattern of decreasing \( E \) under heating is not seen during the recooling. This indicates that the discrete steps relate to dissociation of the hemoglobin quaternary structure, which (as compared to the tertiary and secondary structures) is expected to be the most fragile one. Figure 6 confirms that the event at 49°C takes place in a partially unfolded state.

4. We now face a non-trivial situation: the event happens at the same temperature 49°C for both horse and human hemoglobin. But, the behavior of the Young’s modulus is very different: it suddenly increases for the horse hemoglobin (more rigid structure for higher temperatures), but decreases for human hemoglobin (less rigid). We repeated the experiment with several different samples, to be sure that the difference between human and horse hemoglobin is well reproduced.

It is well known that these two macromolecules differ by 20-25 acid residues on each hemoglobin unit [20]. Due to such differences the horse hemoglobin has lower reactivity with respect to certain cofactors regulating oxygen binding [21].

We conjecture that these biochemical differences are reflected in the mechanical features of hemoglobin around 49°C. The slow degrees that are responsible for the mechanical event at 49°C are most probably the same for the horse and human hemoglobin, otherwise the temperature 49°C could not be the same for both situations. But since the environments of these degrees of freedom in horse and human hemoglobin are different, we get a different overall response for horse and human situations.

5. For temperatures higher than 65°C the Young’s modulus for the hemoglobin crystals [both for human and horse] abruptly decreases again (not shown on figures) indicating on its full denaturation. For such high temperatures we expect that even the secondary structure of the macromolecule is broken. Our experimental samples became unstable for temperatures higher than 70°C, so that no reliable data could be extracted.

6. To gain more evidence on whether the described effect is specific for the tetrameric structure of hemoglobin, we performed the same experiment with the myoglobin crystals and showed the result in Fig. 7. Upon heating, the Young’s modulus \( E \) of the myoglobin decreases gradually, without discrete steps. This is consistent with breaking the tertiary structure of the myoglobin towards acquiring a more labile state. This also confirms that the discrete steps seen in Figs. 6 and 7 relate to the dissociation of the quaternary structure, which is absent for myoglobin. Apart from relatively small non-monotonicity of \( E \) around 57°C, the behavior of \( E \) is monotonic and reversible upon recooling. It is seen though that the reversibility is better visible for \( T > 57°C \) than for lower temperatures, since for low temperatures \( E \) is more influenced by the well-defined myoglobin tertiary structure, which is not completely recovered after recooling. It is known that the calorimetric experiments for myoglobin show a well-displayed transition to a partially denaturated (molten) state, where its tertiary structure is partially lost; see Fig. 8 for further references. Depending on certain experimental conditions this happens around 60°C – 80°C [8]. But the mechanical features of myoglobin do not change suddenly during this transition to the partially molten state. This corresponds to the behavior of the logarithmic decrement of damping for the myoglobin—see Fig. 9—and is consistent with the gradual decrease of \( E \) with temperature; see Fig. 7.

Relations to previous work. Several experimental studies carried out via various methods (calorimetry, optics) on liquid-state samples displayed that something peculiar happens with hemoglobin around 49°C. [8–10]. The authors of [8] and [9] prescribed the 49°C event to the onset of aggregation. As we saw, this is correct, but essentially incomplete: the aggregation indeed starts around 49°C, but there is certainly more there than simply aggregation. Artmann et al. found indications of conformational transitions (not reducible to aggregation) at 49°C using optical methods on liquid state human hemoglobin [10]. This is close to our results. They extensively studied hemoglobin of other species...
and noted that the event correlates with the physiological temperature and relates to the motion of erythrocytes (red blood cells). They also suggested that the scenario of this conformational transition can be similar to the glass transition in polymers. 

Also this suggestion is confirmed by our results, because the peak of the internal friction around transition temperature [see Fig. 5] is a known indication of the glass transition, as was employed recently for detecting the glass transition in collagen [22, 23]; see also [15, 24–27] in the context of glassy features of biopolymers.

Several decades ago it was conjectured that conformational changes related to biopolymer functioning proceed via mechanical motion of certain mesoscopic degrees of freedom [28]. This protein-machine conjecture was taken up in [1], where certain aspects of the low-temperature kinetics of myoglobin were interpreted via proteinquakes: a sudden release of energy accumulated in elastic degrees of freedom. Later on, proteinquakes were found to be relevant for functioning of myosin [10] and adenylate kinase [11]. An important aspect of this research was that proteinquakes were connected to partial unfolding of the biopolymer tertiary structure [10, 11]. This agrees with our finding that the heating-induced proteinquake at 49°C takes place in a partially unfolded state of hemoglobin.

Meanwhile the protein-machine conjecture was supported from another angle: not only the protein functioning resembles that of a machine, but also the performance of an optimal (high efficiency and a large power) heat engine—as described by a generalized Carnot cycle—has shown deep analogies with protein physics and the folding-unfolding transition [29].

Discussion

Our main message is that upon temperature elevation horse and human hemoglobins experience a conformational transition around 49°C detectable via suddenly changing Young’s modulus and decreasing internal friction. We argued that this is a mechanical event and that it cannot be traced back to denaturation and/or aggregation. The precise scenario of the event—but not its temperature—appears to be dependent on the type of hemoglobin. We conjectured that this difference relates to structural differences in the horse and human hemoglobin.

The message of our results for the hemoglobin functioning is that its mechanical features can be triggered by temperature in addition to other pertinent factors such as pH or oxygen concentration. In particular, our results can turn out to be relevant for understanding the process of oxygen release that in tissues which strongly need oxygen should take place much faster than the oxygen consumption in lungs. During the in vitro experiments we naturally do not see those additional factors and thus the temperature has to be larger than the physiological range for seeing the effect.

Note that the global temperatures ≥ 42°C are lethal for humans and horses. However, the local temperature can easily go to values larger than 42°C without causing any serious trouble for living tissues. A pertinent example is the hyperthermia treatment of cancer, where the local temperature goes to values larger than 45–48°C without destroying healthy tissues. Note as well that the orientation of hemoglobin molecules in erythrocytes is not random (in that respect they are similar to protein crystals). First indications of this fact were obtained some 30 years ago, but were not widely disseminated in that time [30]. More recently this fact was confirmed by several independent studies; see e.g. [31].

In conclusion, we reiterate that the main experimental result of this work—proteinquake in heated hemoglobin—can be interpreted as a sudden, temperature-controlled mechanic motion. The mechanic character of this motion is to be compared with the fact that certain features of proteins may well have glassy features. Recall that the glassy state is yet another (different from a mechanic motion) form of non-equilibrium that is characterized by slow relaxation and strong memory effects [32, 34]. By now there are many experimental and numerical indications of such a state in biopolymers [15, 22, 27]. It should be interesting to carry out direct experiments and study in which specific way the glassy state in proteins coexists with the mechanic motion.

Methods.

Materials. Monoclinic crystals of horse and human hemoglobin were grown following the modified method of Drabkin [35]. The solution contained 33 mg/ml oxyhemoglobin, 1% sodium oxalate, 0.9 M potassium phosphate and had pH = 6.5. It was poured on glass weighing cups, which were put inside the crystallization chamber. At the bottom of the chamber we poured a solution of 3% sodium oxalate and 2.7 M potassium phosphate (pH = 6.5). Crystallization was processed under 4–6°C for several months. The crystals came out as thin rhomboids with the length around \( L = 4 \) mm, width \( b = 0.05 \) mm and thickness \( h = 0.005 \) mm (we stress that different crystal samples have slightly different values of \( L, b \) and \( h \), what are given here are the characteristic values). This form did not differ from that described in [35] where the crystallization was processed in the presence of sodium oxalate and \((NH_4)_2SO_4\). The obtained crystals can be utilized directly (without fixation) for our micromechanical experiments. A typical structure is shown in Fig. 2 [16, 17]. Monoclinic crystals of sperm-whale myoglobin were grown following the method [36].
Experimental methods. The dynamic Young’s modulus $E$ and the logarithmic decrement of damping $\theta$ for hemoglobin and myoglobin crystals were studied via the method described in [12, 27]. The method is based on analyzing electrically induced transverse mechanical oscillations of the plate which is fixed by a cantilever. The dynamic Young’s modulus measures the elasticity degree. To measure $E$, one changes smoothly the frequency $f$ of the induced oscillations to determine experimentally the basic resonance frequency $f_0$, which corresponds to the maximal oscillation amplitude of plate’s loose end. The Young’s modulus for the long axial direction of the plate is given as:

$$E = 3.19 \frac{f_0^2 L^4 \rho S}{I},$$

(1)

where $L$ is the length of sample, $S = bh$ is the cross-section area of the plate, $\rho$ is its density, and $I = bh^3/12$ is the main inertia moment of the plate.

The logarithmic decrement of damping $\theta$ is used as a measure of the internal friction, and is defined as $\theta = \ln[A(t)/A(t + T)]$, where $A(t)$ is the oscillation amplitude in time $t$, and $T$ is the period. $\theta$ is measurable by two related methods. One can measure the length of the resonance curve and calculate $\theta$ according to: $\theta = \pi \Delta f/f_0$, where $\Delta f$ is the difference of frequencies between the oscillation amplitude at the maximum amplitude and $\sqrt{2}$ times less than the maximum. A more precise determination method amounts to measuring the phase shifts between the oscillations of exciting force and the sample loose end [15, 37].

[1] Perutz MF (1969) Croonian Lecture 1968 - Haemoglobin molecule. Proc. Roy. Soc. B 173: 113-140.
[2] Eaton WA, Henry ER, Hofrichter J, Mozzarelli A (1999) Is cooperative oxygen binding by hemoglobin really understood? Nature Str. Biol. 6: 351-358.
[3] Bohr C, Hasselbalch K, Krogh A (1904) About a new biological relation of high importance that the blood carbonic acid tension exercises on its oxygen binding. Skandinavisches Archiv fur Physiologie 16: 402-412.
[4] Lukin JA, et al. (1985) Low-temperature glass transition in proteins. Proc. Natl. Acad. Sci. USA 99: 9202-9206.
[5] Terada TP, Sasai M, Yomo T (2002) Conformational change of the actomyosin complex drives the multiple stepping movement. Proc. Natl. Acad. Sci. USA 99: 9202-9206.
[6] Miyashita, O, Omuchi JN, Wolynes, PG (2003) Nonlinear elasticity, proteinquakes, and the energy landscapes of functional transitions in proteins. Proc. Natl. Acad. Sci. USA 100: 12570-12575.
[7] Perutz MF (1953) Polarization dichroism, form birefringence, and molecular orientation in crystalline haemoglobins. Acta Crystallogr. 6: 859-864.
[8] Bourgeois D (2009) Watching CO enmeshed in hemoglobin. Structure 17: 1427-1428.
[9] Starikov EB (1997) Chemical physics of solid-state nucleic acids: New intriguing horizons. Phys. Rep. 284: 2-89.
[10] Morozov VN, Gevorkian SG (1985) Low-temperature glass transition in proteins Biopolymers 24: 1785-1799.
[11] Fermi G, Perutz MF, Shaanan B, Fourné R (1984) The crystal structure of human deoxyhaemoglobin at 1.74 Å resolution. J. Mol. Biol. 175: 159.
[12] From Protein Data Bank at http://www.rcsb.org/pdb/explore.do?structureId=2HbB.
[13] Trinh K (1965) Biology and information, elements of biological thermodynamics (Consultants Bureau, NY).
[14] Bawal BK, Vijayan M (2002) Structures of human oxy- and deoxyhaemoglobin at different levels of humidity: variability in the T state Acta Cryst. D 58: 1155-1161.
[15] Clegg JB, Goodburn SE, Braend M (1984) Genetic organization of polymorphic equine α globin locus and sequence of the BII α1 gene. Nucleic Acids Res. 12: 7847-7858.
[16] Di Giudina B, et al. (1990) Differences between horse and human haemoglobins in effects of organic and inorganic anions on oxygen binding. Biochem. J. 266: 897-900.
[17] Gevorkian SG, Allahverdyan AE, Gevorgyan DS, Hu CK (2011) Glassy state of native collagen fibril? EPL 95: 23001.
[18] Gevorkian, SG, Allahverdyan AE, Gevorgyan DS, Simonian AL, Hu CK (2013) Stabilization and anomalous hydration of collagen fibril under heating. Plos One 8: e78526.
[19] Iben, IET et al. (1989) Glassy behavior of a protein. Phys. Rev. Lett. 62: 1916-1919.
[25] Ma, WJ, Hu, CK (2010) Generalized statistical mechanics and scaling behavior for non-equilibrium polymer chains I: monomers connected by rigid bonds. J. Phys. Soc. Jpn. 79: 024005.
[26] Ma, WJ, Hu CK (2010) Generalized statistical mechanics and scaling behavior for nonequilibrium polymer chains II: monomers connected by springs. J. Phys. Soc. Jpn. 79: 024006.
[27] Hu, CK, Ma, WJ (2010) Molecular Dynamics Approach to Relaxation and Aggregation of Polymer Chains. Prog. Theor. Phys. Supp. 184: 369-384.
[28] Chernavskii DS, et al. (1980) Electron tunneling process and the segment mobility of macromolecules. Proc Natl Acad Sci USA 77: 7218-7221.
[29] Allahverdyan AE, Hovhannisyan KV, Melkikh AV, Gevorkian SG (2013) Carnot cycle at finite power: Attainability of maximal efficiency. Phys. Rev. Lett. 109: 248003-1-5.
[30] Fok MV, Arkhangelskii NB, Zaritskii AR, Prokopenko GA, Faddeev VV (1985) The role of erythrocyte membrane in oxygen delivery to tissues. Preprint of Moscow Physical Institute, number 41.
[31] Wood BR, Hammer L, and McNaughton D (2005) Resonance Raman spectroscopy provides evidence of heme ordering within the functional erythrocyte. Vibrational spectroscopy, 38, 71-78 (2005).
[32] Dasgupta C., Ma SK, Hu, CK (1979) Dynamic properties of a spin glass model at low temperatures. Phys. Rev. B 20: 3837-3849.
[33] Hu C.-K. (2013) Slow dynamics in proteins and polymer chains. AIP Conference Proceedings 1518: 541-550.
[34] Hu C.-K. (2014) Historical review on analytic, Monte Carlo, and renormalization group approaches to critical phenomena of some lattice Models, Chin. J. Phys. 52: 1-76.
[35] Drabkin DL (1946) Spectrophotometric studies XIV: the crystallographic and optical properties of the hemoglobin of man in comparison with those of other species. J. Biol. Chem. 164: 703-723.
[36] Kendrew JC, Parrish RG (1957) The crystal structure of myoglobin. III. Sperm-whale myoglobin. Proc. Roy. Soc. A 238: 305-324.
[37] Morozov VN, Morozova, TYa. (1981) Viscoelastic properties of protein crystals: triclinic crystals of hen egg white lysozyme in different conditions. Biopolymers 20: 451-467.
[38] Landau, LD, Lifshitz EM (1965) Elasticity Theory (Nauka Publishers, Moscow).

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FIG. 1: (Color online) Schematic representation of the hemoglobin quaternary structure with four globular sub-units (yellow color: $\alpha_1, \alpha_2, \beta_1, \beta_2$) and four heme groups (blue color). (Left) T-form, where the access to the oxygen binding parts of the heme groups is restricted and the overall structure is more compact; (Right) R-form with easier access to the heme groups by oxygen molecule O$_2$ and a more loose structure. The cooperativity of hemoglobin during oxygen binding is related to the transition from the T form to the R form.

FIG. 2: (Color online) Contacts between two deoxyhemoglobin molecules in monoclinic crystal at resolution 1.74 Å with parameters $P(1\ 2\ 1)$, $a = 63.15$ Å, $b = 83.59$ Å, $c = 53.80$ Å, $\alpha = 90.0^\circ$, $\beta = 99.3^\circ$, $\gamma = 90.0^\circ$ \cite{16, 17}. Red points represent water molecules from the first Langmuir adsorption layer. The relative humidity is 95%-98%.

FIG. 3: (Color online) The Young’s modulus and the logarithmic decrement of damping of the human hemoglobin under heating. The relative humidity is now 95%.
FIG. 4: (Color online) The Young’s modulus of the horse versus human hemoglobin. Both samples were prepared at the same initial temperature $t = 25^\circ$ and relative humidity 75%. The Young’s modulus at temperature $t = 25^\circ$: $E_{t=25^\circ} = 0.75 \text{ GN/m}^2$ for the horse hemoglobin sample and $E_{t=25^\circ} = 0.94 \text{ GN/m}^2$ for the human sample.

FIG. 5: (Color online) The normalized Young’s modulus $E/E_{t=25^\circ}$ and the logarithmic decrement of damping, $\theta$, versus temperature $t$ for monoclinic crystals of horse hemoglobin. The relative humidity is 75%. The heating rate is $0.1^\circ \text{ C/min}$ and $E_{t=25^\circ} = 0.75 \text{ GN/m}^2$.

FIG. 6: (Color online) The Young’s modulus of the human hemoglobin under heating and re-cooling in the vicinity of $49^\circ$ C. The relative humidity is 95%. The heating rate is $0.1^\circ \text{ C/min}$. Temperature is smaller than $49^\circ$ C and $E_{t=25^\circ} = 0.11 \text{ GN/m}^2$. 
FIG. 7: (Color online) The Young's modulus $E$ versus temperature $t$ under heating and recooling for monoclinic crystals of sperm-whale myoglobin. The denaturation process is seen to be approximately reversible.

FIG. 8: (Color online) The logarithmic decrement of damping, $\theta$ versus temperature $t$ under heating and recooling for monoclinic crystals of sperm-whale myoglobin.