Report of a Workshop on:

**Smooth Particle Hydrodynamics: Models, Applications, and Enabling Technologies**

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Abstract

We present the results from a two-day study in which we discussed various implementations of Smooth Particle Hydrodynamics (SPH), one of the leading methods used across a variety of areas of large-scale astrophysical simulations. In particular, we evaluated the suitability of designing special hardware extensions, to further boost the performance of the high-end general purpose computers currently used for those simulations. We considered a range of hybrid architectures, consisting of a mix of custom LSI and reconfigurable logic, combining the extremely high throughput of Special-Purpose Devices (SPDs) with the flexibility of reconfigurable structures, based on Field Programmable Gate Arrays (FPGAs).

The main findings of our workshop consist of a clarification of the decomposition of the computational requirements, together with specific estimates for cost/performance improvements that can be obtained at each stage in this decomposition, by using enabling hardware technology to accelerate the performance of general purpose computers.

The decomposition of astrophysical SPH applications is characterized by four modules:

1) Most compute-intensive in any code is the module that computes the pair-wise gravitational interactions;

2) The naive \( N^2 \) force count, in a self-gravitating system of \( N \) particles, can be reduced to \( N \log N \) scaling, at the expense of considerable computational overhead;

3) The third-most computationally intensive module is the one performing SPH;

4) The remaining few percent of the total computational cost is taken up by modeling additional physics, such as radiative transport and other non-gravity/hydro effects.

For the specific case of large-scale cosmological simulations, a leading application of SPH in astrophysics, we arrived at the following estimates of cost/performance improvements that can be made by utilizing a combination of SPD and FPGA accelerator technology.

- For \( N^2 \) gravity, a cost/performance improvement of a factor 1000 can be achieved (and will be achieved in the year 2000, by the 100 Tflops GRAPE-6 SPD, under development at the University of Tokyo, through a grant from the Japanese Ministry of Education).

- More efficient \( N \log N \) algorithms can be implemented as hardware accelerators (e.g. as SPD chips for the Ewald method, or an FPGA subsystem for a Barnes-Hut tree), leading to a cost/performance improvement of a factor 100.

- In addition, SPH hardware could be developed (either as SPD or FPGA subsystems), which would lead to an estimated cost/performance improvement of a factor 50, for the net speed-up of simulations including both gravity and SPH, compared to running the same simulation with the most efficient code on the general-purpose front-end.

- For a full state-of-the-art simulation of the origin of large-scale structure in the universe, additional physical processes would need to be modeled on the front-end. Full throughput simulations would then achieve a net cost/performance improvement factor estimated to lie in the range 20 \( \sim \) 30.
1. Introduction

This report summarizes the conclusions that were reached during a two-day workshop on "Smooth Particle Hydrodynamics: Models, Applications, and Enabling Technologies", at the Institute for Advanced Study in Princeton, June 19-20, 1997.

The workshop took place in the larger context of a series of meetings, devoted to the exploration of pathways to petaflops computing. Of the four main architecture categories, identified as candidates for designing a petaflops computer during previous workshops, three have a general-purpose character. The fourth category pertains to Special-Purpose Devices (SPDs). Currently, the SPD with the highest speed is the GRAPE-4, developed at the University of Tokyo. The GRAPE-4 is designed to speed up gravitational \( N \)-body calculations that form the core of many simulations in astrophysics.

The name GRAPE stands for GRAvity PipE, and indicates a family of pipeline processors that contain chips specially designed to calculate the Newtonian gravitational force between particles. A GRAPE processor operates in cooperation with a general-purpose host computer, typically a normal workstation. The force integration and particle pushing are all done on the host computer, and only the inter-particle force calculations are done on the GRAPE. Since the latter require a computer processing power that scales with \( N^2 \), while the former only require \( \propto N \) computer power, load balance can always be achieved by choosing \( N \) values large enough.

The Grape-4 developers have won the Gordon Bell prize for high-performance computing in each of the past two years. In 1995, the prize was awarded to Junichiro Makino and Makoto Taiji for a sustained speed of 112 Gflops, achieved using one-sixth of the full machine on a 128k particle simulation of the evolution of a double black-hole system in the core of a galaxy. The 1996 prize was awarded to Toshiyuki Fukushige and Junichiro Makino for a 332 Gflops simulation of the formation of a cold dark matter halo around a galaxy, modeled using 768k particles on three-quarters of the full machine.

In December 1995, we held a one-day workshop at NCSA, in order to discuss possible future developments for the use of SPDs in astrophysics. Extending the teraflops class GRAPE-4 to a petaflops class next-generation machine was seen to be a real possibility by the year 2000. In addition, we discussed ways to extend the functionality of these SPDs beyond the simulation of purely gravitational calculations. In particular, the idea was suggested to make a hardware implementation of one of the most popular algorithms for hydrodynamics in astrophysics, SPH (Smooth Particle Hydrodynamics).

Unlike more conventional grid-based codes, an SPH code is a type of \( N \)-body code, in which each particle carries with it thermodynamic information (such as the entropy), in addition to the usual values for its mass, position, and velocity. Each particle determines its local hydrodynamical conditions through an averaging procedure that involves a number of nearest neighbors. A variety of algorithmically different versions of SPH exist. For example, there is a large amount of freedom in the choice of kernel that can be used for smoothing purposes, in order to extract the local thermodynamic quantities from the values carried around by neighboring particles.
At the start of the workshop, during the morning session of the first day, the following brief review talks were presented.

Lars Hernquist presented an overview of SPH. He discussed the role played by SPH modeling in large-scale simulations in astrophysics. He presented a comparison between different SPH approaches, and a comparison with non-SPH versions of hydrodynamics.

Thomas Sterling spoke about the future role of special-purpose devices. He gave a summary of the petaflops initiative and discussed future directions for high-performance computing. In addition, he talked about the role that special-purpose devices can be expected to play.

Jeff Arnold gave an overview of the SPLASH-2 project. This project provided the first large-scale example of a high-speed computer based purely on FPGAs (Field-Programmable Gate Arrays, a form of reconfigurable logic). He presented a brief history of the project, discussed lessons learned from it, and mentioned some future prospects.

Piet Hut presented an overview of the GRAPE project, past and future. He gave a summary of the 8-year history of the project, and listed the characteristics of the different GRAPE models. He then reviewed some of the science done on them, and discussed projected future developments.

Steve McMillan talked about plans and possibilities for the GRAPE-6, the planned petaflops version of the teraflops GRAPE-4. He gave an outline of some ideas to combine the GRAPE-6 pure-gravity hardware with a 1-10 Tflops FPGA system for modeling non-gravitational physics.

During the afternoon session of the first day, and throughout the second day, various round-table discussions were held, in order to go deeper into the questions that were raised during the presentations listed above. Specifically, we concentrated on the following list of questions, provided by Thomas Sterling in his talk:

- Science — Using SPH within certain performance regimes, what new science will be enabled.
- Model — To what degree is SPH a valid representation of the physical phenomena to be modeled? Where does it work, where will it fail?
- Forms — What is the range of variations of SPH that must be incorporated and how may they be parametrized?
- Performance — What is the computational demand with respect to science problem and problem size.
- Impact — How does computational SPH affect performance scaling of entire science problem?
- Data Flow — What are the data flow rates across the SPH interface and how does this scale with problem size and with respect to other computational components (N-body simulation, etc.)
• Implementation — Does an SPD approach provide significant performance advantage for SPH over alternative computational methods? Is a reconfigurable logic methodology suitable?
• Plan — What is needed? What will it cost? How long will it take?

The remainder of this report illustrate the main findings, in response to these questions.

The scientific organizing committee for the workshop consisted of the following six members:

Piet Hut (chair, Institute for Advanced Study, Princeton)
Lars Hernquist (Lick Observatory, University of California, Santa Cruz)
George Lake (Astronomy Department, University of Washington, Seattle)
Jun Makino (Department of General Systems Study, Komaba, University of Tokyo, Japan)
Steve McMillan (Department of Physics and Atmospheric Science, Drexel University, Philadelphia)
Thomas Sterling (Jet Propulsion Laboratory, Pasadena & California Institute of Technology, Pasadena)

In total, there were 19 participants. In additions to the ones listed above, the following individuals attended the workshop:

Jeff Arnold (independent consultant)
Romeel Davé (Astronomy Department, University of California, Santa Cruz)
Kimberly Engle (Department of Physics and Atmospheric Science, Drexel University, Philadelphia)
Toshiyuki Fukushige (Department of General Systems Study, Komaba, University of Tokyo, Japan)
Neal Katz (Dept. of Physics and Astronomy, University of Massachusetts, Amherst)
Nobuyuki Masuda (Department of Earth science and Astronomy, Komaba, University of Tokyo, Japan)
Julio Navarro (Steward Observatory, University of Arizona, Tucson)
Mike Norman (Department of Astronomy, University of Illinois, Urbana)
Kevin Olson (George Mason Univ. and NASA/GSFC, NASA/GSFC, Greenbelt)
Matthias Steinmetz (Steward Observatory, University of Arizona, Tucson)
Frank Summers (Columbia Astrophysics Lab, Columbia University, New York)
Peter Teuben (Astronomy Department, University of Maryland, College Park)
James Wadsley (CITA/Department of Astronomy, University of Toronto, Toronto, Canada)
2. Smooth Particle Dynamics: the Computational Challenge

There are a number of excellent review articles describing SPH in depth, particularly that due to Monaghan (1992; ARA&A 30, 543). What follows is a cursory survey of the method, emphasizing the challenges that face designers of special-purpose hardware.

Smoothed particle hydrodynamics was originally formulated by Lucy (1977; AJ 82, 1013) and Gingold & Monaghan (1977; MNRAS 181, 375) to model self-gravitating fluids in astrophysics. Unlike traditional Eulerian algorithms, SPH represents a fluid with particles and does not require a grid to integrate the equations of motion. This feature makes SPH ideal for situations were a large dynamic range is needed or systems where the “interesting” parts of the fluid occupy only a small fraction of the simulation volume. It has been applied with success to problems ranging from astronomical impacts and stellar collisions to galaxy mergers and the formation of large-scale structures in the Universe. The ease with which other physical processes can be incorporated into SPH codes also makes this method well-suited for modeling phenomena outside the astronomical realm, including nuclear dynamics, MHD instabilities, the dynamics of solids, and free surface flows.

Intuitively, SPH describes a fluid by replacing its continuum properties with locally averaged (smoothed) quantities. In this sense, the formal development of SPH is not unlike the mathematical theory of generalized functions. Local averages are performed by dividing the fluid into elements which carry a certain mass and then replacing integral quantities by discrete sums over the mass elements. For example, the locally averaged density in SPH is given by expressions of the form

\[
\langle \rho(r) \rangle \approx \sum_{j=1}^{N} m_j W(r - r_j, h),
\]

where the angle-brackets imply that the density has been smoothed over a region whose extent is determined by the “smoothing kernel” \( W(r, h) \) over the characteristic length-scale, \( h \). Formally, the estimate provided by equation (1) is equivalent to summing over \( N \) particles each having a density profile determined by the smoothing kernel. A real fluid can also be imagined to consist of fluid “particles” provided that these particles are small compared to the scales over which macroscopic properties of the fluid varies, but large enough to contain many molecules so that macroscopic averages can be defined sensibly. In an SPH computation, the number of simulation particles is necessarily small and, hence, the averaging scale, set by \( h \), may not always be small compared to the distance over which the fluid property varies. This fact emphasizes the need for large numbers of particles in the calculations, since the exact continuum limit is recovered only as \( N \to \infty \).

The procedure just described is analogous to that used to formulate a discrete (N-body) version of collisionless dynamics. Similar to that development, smoothing in SPH
can be extended to any physical property and can be applied to derive equations of motion for the fluid that reduce to the Navier-Stokes equations for a sufficiently large number of fluid elements. Computationally, as in an N-body algorithm, SPH codes follow the motions of particles which, in addition to their mass, carry the hydrodynamic and thermodynamic information needed to specify the evolution of the fluid. Thus, particles in SPH are like nodes in a mesh, but one that is continuously deformable and distorts automatically to put more of the computational effort in regions of relatively high density. Gradients are calculated from the smoothing procedure, which makes it possible to interpolate between particles.

A number of practical issues must be addressed before the functionality of SPH can be hardwired. The choice of the smoothing kernel is not unique, although it is desirable to employ a form such that \( W \) is sharply peaked, to preserve the local character of the smoothing process. In some cases, it may prove advantageous to employ an anisotropic smoothing kernel, depending on the symmetry of the flow. Regrettably, there is no formal theory for error propagation in SPH, because the rate of convergence of the smoothed estimates depend on how the particles are distributed and how they evolve, and so it is not possible to select the optimal smoothing kernel a priori. (The same would be true for a mesh-based code in which the grid points are free to move with the fluid in an arbitrary manner.) The discrete form of the equations of motion is not unique and various choices lead to forms that propagate errors slightly differently, depending on the particle number. Usually, it is advantageous to give each particle its own smoothing length, and to allow smoothing lengths to vary dynamically as the structure of the fluid changes. In this case, the form of the equations of motion is again not unique, and neither is the prescription used to update smoothing lengths from one timestep to another. Finally, SPH requires an artificial viscosity to capture shocks. The best choice for the artificial viscosity is not known, and it may, in fact, be application-dependent.

In a sense, all these ambiguities are issues of “detail” and it could be the case that differences introduced by variations in things like the smoothing kernel would be unimportant in the limit where the particle number were multiplied by a factor of, say 100 relative to what is currently feasible. Perhaps a more serious problem confronting the development of special purpose hardware for SPH is the need to include additional physical processes and the reality that the extra physics will vary widely from one application to another. When applied to cosmology and galaxy formation, for example, SPH codes must handle the interaction between the gas and background radiation fields, follow the ionization state of the gas, and account for the effects of star formation and feedback. Applications to the interstellar medium require a treatment of magnetic fields in the gas, account for diffusive processes on small scales, and contend with the structure of a multi-phase medium. Even more exotic effects may be needed to model, for example, mergers of compact and ordinary stars, such as nuclear burning and general relativity. Designing hardware that would be both computationally efficient yet sufficiently flexible to be easily adaptable to include all these physical processes would appear to be a formidable challenge indeed.
3. Issues and Opportunities

- **Science** — Using SPH within certain performance regimes, what new science will be enabled?

In astrophysics, most hydrodynamics applications span many orders of magnitude in density. This makes a straightforward application of a non-adaptive grid code very inefficient. 3-D Lagrangian grid codes, or codes using a hierarchy of adaptive grids, are still largely under development. SPH, in contrast, is fully 3-D and has been widely used in astrophysics for more than ten years. It is an intrinsically adaptive algorithm, since lower densities are simply reflected in wider particle spacing.

Current applications of SPH span a wide range of astrophysical regimes, from planetary formation and the dynamics of interstellar matter to the behavior of interacting galaxies and the large-scale structure of the expanding universe. Increasing the speed of those calculations will benefit all these areas. Certain critical problems in these areas require simulations with spatial and/or temporal resolution substantially beyond what is presently available, and even beyond what is anticipated to become available within the next few years.

The desired resolution in an SPH simulation determines the number of SPH particles required. The cost of a typical calculation (including gravity) scales somewhat faster than the total number of particles. Particle numbers in the range $1 \times 10^6$ are currently feasible. For problems such as encounters between individual stars or individual galaxies, this allows fairly detailed modeling of global behavior. For a resolution of local detail, however, such as interactions between individual molecular clouds in galaxy—galaxy collisions, or galaxy structure and interactions in cosmological simulations, more than $10^8$ particles will be needed. Such calculations will require computer speeds in the petaflops domain.

- **Model** — To what degree is SPH a valid representation of the physical phenomena to be modeled? Where does it work, where will it fail?

In the limit of very large particle number, the SPH equations reproduce the Navier-Stokes equations of fluid dynamics. In this sense, SPH has been proven to be correct. In practice, the adequacy of SPH strongly depends on the particular problem under consideration. For example, an accurate simulation of shocks will require a much larger particle number than a model in which the fluid flows are more smooth. The method’s scaling and error properties are still the subject of active research.

A substantial increase in the number of particles in a simulation will likely have to be accompanied by the inclusion of a significantly greater degree of physical detail, such as radiative transfer, magnetic fields, ionization and cooling, and a treatment of multi-phase media. Perhaps the most challenging problem in large-scale simulations is to provide an
adequate treatment of star formation. Here, the computational speed-up will help, but there still remain several unresolved issues concerning the physical effects involved.

- **Forms** — What is the range of variations of SPH that must be incorporated and how may they be parametrized?

During the twenty years since the first appearance of SPH, a wide variety of algorithms and implementations has appeared in the literature. It is fair to say that currently almost every individual researcher has his or her favorite method, differing in several aspects from those of their colleagues. The major areas of divergence among current SPH implementations are: (1) the choice of smoothing kernel, (2) the choice and specification of smoothing length, (3) the symmetrization of the equations of motion, (4) the form of the artificial viscosity term used to handle shock propagation and (5) the form and implementation of the energy equation.

While we discussed these differences, it became clear that considerable speed-up would entice most SPH researchers to give up their own favorite scheme in order to use the scheme implemented in the fast hardware. Therefore, the current variation in implementations should not stand in the way of a special-purpose implementation of SPH. However, it was also clear that handling a lot of “new” physics on the front end would substantially reduce the overall speedup achieved.

- **Performance** — What is the computational demand with respect to science problem and problem size.

Gravity plays an important role in all astrophysical applications of SPH, making it impossible to separate the gravitational physics from the hydrodynamics in any practical way. Thus, analysis of computational demand necessarily requires that both components of the problem be considered together. In many cases, the computation of the gravitational force provides essential information (such as neighbor lists) for the SPH calculation. A further complication for cosmology is the fact that periodic boundary conditions must be applied, increasing by a non-negligible factor the cost of tree-based gravitational force calculations.

In a “typical” tree-based cosmological code, the breakdown of computational effort among the various parts of the program is as follows: (1) tree construction and traversal (including neighbor list determination), 20%; (2) computation of gravitational interactions, 70% (20% of this associated with the implementation of periodic boundary conditions); (3) SPH force calculation, 10%.

We will analyze the impact of SPDs on these components separately, although we recognize that separating the functionality into two or more distinct hardware components may incur a substantial bandwidth penalty in communicating results among the various parts of the system. Note that it makes sense to speed up the SPH calculation only if steps are first taken to accelerate the gravity and tree-handling portions of the code.

- **Impact** — How does computational SPH affect performance scaling of entire science problem?

In currently existing codes, running on workstations or moderately parallel machines, SPH
implementations are highly intertwined with the treewalk part of the gravity calculations. Together, they make up roughly one third of the computational expense. If the gravity part of the calculation were sped up by the use of SPDs, the SPH calculations would become the bottleneck, limiting the overall speed-up to only one order of magnitude, irrespective of how fast the gravitational calculations could be performed.

If, however, the SPH part could be implemented in hardware, in SPD or FPGA form, then the net speed-up would be significantly greater. The overall speed would then be determined by the next bottleneck—the additional physics, such as radiative transport and cooling, mentioned above. More detailed estimates are presented in the table below.

- **Data Flow** — *What are the data flow rates across the SPH interface and how does this scale with problem size and with respect to other computational components (N-body simulation, etc.)*

Considering just the SPH subsystem, calculation of the SPH portion of the force on a single particle requires that $\sim 100$ neighbor interactions be computed, at a cost of about 100 floating-point operations per interaction. The total amount of particle data required (for the particle under consideration, not its neighbors) is on the order of 100 bytes. The minimum bandwidth thus is $\sim 0.01$ bytes/flop, or 100 Gbyte/s for a 10 Tflops SPH system. However, this calculation assumes that there is no overhead involved in obtaining and maintaining the required neighbor information, which is unrealistic. There was no discussion of ways in which neighbor information might be transferred efficiently between the gravity and the SPH subsystems.

- **Implementation** — *Does an SPD approach provide significant performance advantage for SPH over alternative computational methods? Is a reconfigurable logic methodology suitable?*

For the pure SPH problem, it appears that a hardware implementation of SPH could produce a substantial improvement in speed, although the I/O issues just described remain unresolved. Whether an algorithm as complex as a typical SPH force loop can be implemented in hardware is unclear. Whether custom or reconfigurable hardware is chosen, it appears that a significant reduction in precision would be necessary in order to fit an SPH pipeline into a chip. The possibility of using multiple FPGAs to implement a single pipeline was discussed briefly, and may be feasible.

There was disagreement as to whether reduced (i.e. less than 32-bit) precision was adequate. The statistical errors inherent in using only 100 neighbors to determine fluid quantities seem to imply that only a few decimal digits of accuracy are actually needed; however, some SPH users maintained that (presently unimplemented) SPH applications involving magnetic fields would require full double precision. No consensus was reached on this issue.

- **Plan** — *What is needed? What will it cost? How long will it take?*

For a 100 Tflops pure gravity engine, the estimated cost is $\sim \$2$ million. The cost of a 10 Tflops SPH subsystem implemented in reconfigurable hardware would probably be similar.
The gravity engine has been funded by the Japanese government and should be completed by 2000. Implementation of SPH in FPGAs could possibly be carried out in a similar timeframe, but only with significant input from the SPH user community.

An important side effect of the construction of a 100/10 Tflops gravity/SPH system would be the availability of single-board workstation accelerators for use by individual researchers, offering 1/0.1 Tflops performance at modest cost (less than $50,000, say). However, the development costs of the gravity and SPH hardware cannot be justified on the basis of these small systems alone.

4. Findings

As mentioned above, the total computational cost of a typical cosmological SPH code using a Barnes-Hut tree for the gravity computation, consists of several basic components: computation of pairwise gravitational interactions (with cost scaling as $O(N)$, where $N$ is the number of particles involved), tree construction and traversal (reducing the gravitational cost to $O(\log(N))$), inclusion of periodic boundary conditions (the so-called “Ewald” method), and the computation of fluid properties using SPH. The workshop’s conclusions on the likely speed-up that might be achieved by hardwiring some or all of these components are summarized in the table below.

|           | $O(N)$ | Tree | Ewald | SPH | Full |
|-----------|--------|------|-------|-----|------|
| $O(N)$    | 1,000  | 20   | 5     | 2   | 2    |
| Tree      |        | 100  | 5     | 2   | 2    |
| Ewald     |        |      | 100   | 5   | 4    |
| SPH       |        |      |       | 50  | 20   |

The top line of the table lists the various applications. (The final application, simply labeled “Full,” assumes that more complex physics, such as heating and cooling, and radiative transport, are also included.) The list is cumulative—each item assumes the use of all items to its left. The left-most column lists the part of the calculation that is presumed to be hard-wired. Again, this list is cumulative—each row presumes that all rows above it are hard-wired. The numbers indicate the improvement in performance that might be achieved over a state-of-the-art general-purpose system in 2001, using the custom and reconfigurable devices expected to be available in that year, operating in tandem with a general-purpose host.
5. Conclusions and Recommendations

1. Hardwiring SPH is feasible, if we can accept a standard algorithm and can live with reduced precision. The former appears to be the case, the latter is less clear. We note also that SPH is probably the most complex astrophysical application we would consider implementing with the technology likely to be available within the next five years.

2. The speedup achieved would be significant, but not overwhelming. Furthermore, it can be achieved only if other more costly components of the calculation are handled first.

3. Significant challenges exist in designing the architecture of a petaflops-class system combining special-purpose gravitational and SPH components. In particular, the dataflow problem associated with neighbor interactions is serious and unresolved.

4. While considerable interest was expressed by SPH users in the possibility of obtaining teraflops-class systems derived from the larger system, the significant development time and expense of both hardware and software mean that such applications alone do not provide sufficient grounds for this project.

5. It is futile to undertake such an extensive project without the active participation of at least some part of the potential user base. At present, there does not seem to be a critical mass within the SPH community to go this route.

6. Hardwiring the log N gravity part will give very significant improvement in cost-performance ratio, of order a factor 100 over general-purpose high-performance computers. This may be a better route to take, leaving SPH to be computed on the front end, and opening up the possibility of extremely fast execution of a large number of non-SPH pure-gravity problems.

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