Stimulated decelerating of diatomic molecules on multiple rovibrational transitions with coherent pulse trains

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We propose a method of stimulated laser decelerating of diatomic molecules by counter-propagating $\pi$-trains of ultrashort laser pulses. The decelerating cycles occur on the rovibrational transitions inside the same ground electronic manifold, thus avoiding the common problem of radiative branching in Doppler cooling of molecules. By matching the frequency comb spectrum of the pulse trains to spectrum of the R-branch rovibrational transitions we show that stimulated cooling can be carried out on several rovibrational transitions simultaneously, thereby increasing number of cooled molecules. The exerted optical force does not rely on the decay rates in a system and can be orders of magnitude larger than the typical values of scattering force obtained in conventional Doppler laser cooling schemes.

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While laser cooling is one of the key techniques of modern atomic physics [1–3], neutral molecules are notoriously challenging to cool to ultracold temperatures. To accomplish this feat one must exercise precise control over a multitude of internal degrees of freedom. A breakthrough in molecular cooling techniques — even for diatomic molecules — is anticipated to enable substantial progress in quantum information processing [4], matter-wave interferometric sensors [5], quantum-controlled chemical reactions [6] and precision measurements [7–9].

To date, the coldest samples of diatomic molecules were obtained by assembling them from ultracold atoms via photo- or magneto-association. This approach produces a gas of ground-state polar molecules near quantum degeneracy [10]. However, so far only bialkali molecules have been produced in this way, and the number of molecules produced is fairly small ($\sim 10^4$). Direct laser cooling of molecules could yield substantially larger samples for a wider range of species.

In traditional Doppler cooling the radiative force originates from momentum transfer to atoms from a laser field and subsequent spontaneous emission in random directions. Repeating this optical cycle tens of thousands of times can slow down thermal beams and cool atomic samples down to the Doppler limit (typically mK). Unfortunately, most atoms and all molecules can radiatively decay to a multitude of states. Exciting population from all these lower-energy states requires a large number of lasers, which makes the conventional scheme impractical. Only for a narrow class of molecules with highly-diagonal Franck-Condon overlaps (i.e., “near-cycling” electronic transitions), this branching problem can be mitigated [11–12].

Here we explore an alternative: employ absorption and stimulated emission on weak transitions inside the same molecular electronic manifold. The concept of “stimulated cooling” was put forward by Kazantsev [13] in 1974; he proposed illuminating a two-level atom with a sequence of alternatively directed and oppositely detuned $\pi$ pulses. For an atom initially in the ground state, a $\pi$-pulse impinging from the left would drive the population upward, while the $\pi$-pulse from the right cycles the population back to the ground state. The net change of atomic momentum is twice the photon recoil momentum $p_r = \hbar k_c$, where $k_c$ is the laser wave-vector. The advantage of this scheme over Doppler cooling is that the momentum transfer can occur much faster than the radiative decay; this is crucial for the use of rovibrational transitions, for which Doppler cooling is impractical due to the very long radiative lifetimes. Stimulated cooling with counter-propagating $\pi$-pulses was explored in a number of works [14–16]. Closely related to the stimulated cooling by $\pi$-pulses is bichromatic force cooling [17–24]. Here the trains of Kazantsev’s $\pi$-pulses effectively arise from the beating of two CW lasers of different frequencies. While the experiments so far have been limited to atoms, bichromatic force cooling of diatomic molecules on near-cycling electronic transitions was recently proposed [25].

In this work we explore molecular slowing with coherent pulse trains. Pulse trains offer several advantages. First, the broadband structure of mode-locked lasers allows one to address multiple rotational levels simultaneously. Secondly, it simplifies stabilization of the multiple frequencies involved, even for species for which building reference cells is impractical [26]. Finally, by manipulating the phases of successive pulse trains, as shown below, the capture range of velocities addressed can be tuned. Looking at the state-of-the-art frequency combs (FC) [27–30], we note that a fiber-laser-based FC with 10 W average power was demonstrated [27] and the authors argue that the technology is scalable above 10 kW average power. The spectral coverage was expanded from optical frequencies to ultraviolet and to mid-IR spectral regions [28–30]. The high resolution quantum control via the combination of pulse shaping and frequency comb was shown in [31–34]. The experiments on line-by-line addressing have been done [32].
We focus on the transitions between the rovibrational levels \((\nu, J)\) inside the ground electronic potential. The frequencies \(\nu_{J,J+1}^{\nu',\nu}\) of the \(R\)-branch \((J \rightarrow J' = J + 1)\) electric-dipole-allowed transitions between rovibrational manifolds read

\[
\nu_{J,J+1}^{\nu',\nu} \approx \nu_{0,1}^{\nu',\nu} + (3B_{\nu'} - B_{\nu})J + (B_{\nu'} - B_{\nu})J^2, \tag{1}
\]

where \(\nu_{0,1}^{\nu',\nu}\) is the frequency of the \(X(\nu, J = 0) \rightarrow X(\nu', J' = 1)\) transition and \(B_{\nu}\) are the rotational constants for the \(\nu\)-th vibrational level \([35]\). This pattern matches the frequency comb (FC) spectrum which consists of a series of sharp equidistant peaks (teeth) located at

\[
\nu_n = \nu_c + \nu_{\text{rep}} \times n - \frac{\Phi}{2\pi T}, \tag{2}
\]

where \(n\) is an integer number, \(\nu_c\) is the carrier frequency, the teeth-spacing \(\nu_{\text{rep}} = 1/T\) is defined in terms of pulse repetition period \(T\), and \(\Phi\) is the carrier-envelope-offset (CEO) phase. We will focus on the \(\nu = 0 \rightarrow \nu' = 1\) transitions. The molecular and the comb spectra could be matched by choosing \(\nu_c = \nu_{0,1}^{0,1}\) and \(\nu_{\text{rep}} = (3B_1 - B_0)/n'\), with \(n'\) being an integer. The \(R\)-branch spectrum becomes Doppler-shifted for moving molecules; we will adjust \(\Phi\) to follow the Doppler shift of the band-head frequency.

As an example, consider the LiCl molecule; here \(\nu_c \approx 19.29\ \text{THz}\) with \(T = 0.95\ \text{ns}\) for the number of teeth between nearly rovibrational transitions \(n' = 40\). For the PbO molecule, \(\nu_c \approx 21.63\ \text{THz}\) with \(T = 0.98\ \text{ns}\) for \(n' = 15\).

Based on these observations we propose the following scheme of stimulated cooling of molecules with pulse trains. As illustrated in Fig. (a), the essential idea is to replace each of the Kazantsev’s \(\pi\)-pulses by a train of \(N\) pulses, each of pulse area \(\theta = \pi/N\). Interference of molecular probability amplitudes induced by the pulses leads to a frequency-dependence of the cooling force resembling the FC spectrum. Cooling will occur simultaneously on several rovibrational transitions. The elementary cooling sequence (or cycle) will consist of two subsequent counter-propagating \(\pi\)-trains. Each cycle will transfer twice the recoil momentum \(p_r = \hbar \nu_c\). To maximize the optical force we assume that the time delay between trains is negligible.

For a moving molecule, Doppler shifts due to the co- and counter-propagating trains have opposite signs. The counter-propagating/upward-stimulating train must be tuned below the resonance and the co-propagating train above the resonance. This can be attained by keeping the carrier frequencies of the two trains the same but having two different CEO phases.

Before proceeding to the full analysis, note that the spectrum given in Eq. (1) is for the \(R\)-branch. To avoid driving \(P\)-branch transitions, one would need to eliminate the low-frequency \((n < 0)\) half of the comb spectrum in Eq. (2), thus reducing the problem to a collection of (separate) two-level systems. This truncation may be accomplished by installing a dispersive element and a static mask at the output of the cavity; the mask would cut out a predefined spectral window. Such a technique has been used by the Orsay group \([36]\) in pulsed laser cooling of Cs\(_2\) molecules.

Furthermore, we would like to avoid driving the \(\nu = 1 \rightarrow \nu = 2\) transitions, see Fig. (b). Fortunately, due to anharmonicity, \(\nu_{0,1}^{1,2} < \nu_{0,1}^{0,1}\), so the \(\nu_{1,2}\) band-head is shifted to lower frequencies, already masked out. Thereby only the higher-\(J\) rotational transitions will overlap with the truncated comb spectrum. The maximum \(J\) of the \(\nu = 1 \rightarrow 2\) band overlapping with the comb spectrum could be estimated as \(J_{\text{max}} = (\nu_{0,1}^{1,2} - \nu_{0,1}^{0,1})/(B_2 + B_1) \approx \nu_c x_c/B_c\), where we used the conventional spectroscopic notation \([35]\). For LiCl and PbO, this limits us to \(J < 6\) and \(J < 10\) correspondingly. This limitation to low \(J\) is consistent with our neglect of higher-order non-rigid-rotor terms in Eq. (1). This limitation is of little consequence: at temperatures below 300 K, the majority of the molecular population is in these low-\(J\) levels. Another peculiarity is that dipole matrix elements vary across rovibrational transitions, while the trains must execute the full \(\pi\) rotation for all transitions simultaneously; to meet this requirement pulse shapers would need to be used so that the Rabi frequency of various transitions remains the same.

**Formalism.** – Since the FC fields couple only pairs of molecular levels, the problem is reduced to finding the time evolution and optical force on a two-level system. Due to the rapid nanosecond time-scale of \(\pi\)-train cycles we may neglect slow radiative decay of the vibrational levels (relevant lifetimes are on the order of a millisecond). We also approximate short non-overlapping laser
pulses by \(\delta\)-functions. In this limit, the pulses are fully characterized by the pulse area \(\theta\) and phase \(\Phi\).

In the interaction picture, the propagator \(U_{\text{train}}\) for a train of \(N\) pulses may be decomposed into a product of propagators due to individual pulses \(U_p\): \(U_{\text{train}} = U_N \ldots U_2 U_1\). The pre-train \((t = t_0^-)\) and post-train \((t = t_0^+ + NT)\) values of the density matrix are related as \(\rho (t_0^+ + NT) = U_{\text{train}} \rho (t_0^-) U_{\text{train}}^\dagger\). The propagator across the \(p^{th}\) pulse may be found analytically \([37]\): \(U_p = i \cos (\theta/2) + i \sigma_p \sin (\theta/2),\) with \(\sigma_p = \sigma_x \cos \eta_{L,R}(t_p) - \sigma_y \sin \eta_{L,R}(t_p)\), where \(\sigma_{x,y}\) are the Pauli matrices. Here \(t_p\) is the arrival time of the \(p\)-th pulse and \(L\) (left) and \(R\) (right) label the co- and counter-propagating \(\pi\)-trains in Fig. 2(a).

The phase \(\eta_{L,R}(t) = \Phi + k_c z(t)\) is the cumulative phase of the laser field experienced by the moving molecule, \(z(t) \approx vt\). Forcing on a target velocity \(v_0\), we may redefine \(\Phi^{L,R}(t) = (\delta + k_c v_0(t)) t + \Phi^{L,R}(t)\), where \(\Phi^{L,R}(t)\) is the control phase that we will tune to optimize the cooling process. Then

\[
\eta_{L,R}(t) = \mp k_c (v - v_0(t)) t - \Phi^{L,R}(t).
\] (3)

At this point we have a prescription for evolving the density matrix over time. The last needed ingredient is the expression for the mechanical momentum transferred to the two-level system. The fractional momentum kick due to a single train may be expressed in terms of the excited state population difference at the end and at the beginning of the train \(-\Delta p_{\text{cycle}}/p_r = \rho_{ee} (t_0^+ + NT) - \rho_{ee} (t_0^-)\) \([37]\).

For the elementary cycle

\[
\frac{\Delta p_{\text{cycle}}}{p_r} = \rho_{ee} (t_0^+ + 2NT) + \rho_{ee} (t_0^-) - 2 \rho_{ee} (t_0^+ + NT).
\] (4)

First of all, \(\Delta p\) is a periodic function, reflecting the underlying periodicity of the FC spectrum. The transferred momentum spikes at values of the phase which are multiples of \(2\pi\). At these points the maximum transferred momentum is limited to twice the recoil momentum, as expected from Eq. (1). This happens only when during the cycle the system starts and ends in the ground state, with a full transfer of the population to the excited state by the first train, i.e., when the \(\pi\)-train conditions are satisfied. Qualitatively, at such values of the phase the probability amplitudes transferred by subsequent pulses interfere constructively.

The detailed profile of the momentum transfer shown in Fig. 2(b) depends on the number of pulses inside \(\pi\)-trains and the number of cycles. For a fixed number of pulses the calculated profile displays a very complicated substructure resulting from intricate interferences of probability amplitudes driven by the multitude of pulses. In accord with the time-frequency uncertainty principle, as the number of pulses grows larger, the peaks become narrower effectively reducing the capture velocity range to zero. Because of this effect, it is natural to wonder how to increase the number of cooled molecules at the end of the process. This goal can be attained by imposing phase relation between the last and the first pulses of two subsequent \(\pi\)-trains:

\[
\Phi^{L,R}_e (t_{M+1,1}) = -\Phi^{L,R}_e (t_{M,N}) + \pi.
\] (5)

Here \(t_{M,n}\) is the arrival time of the \(n\)-th pulse of the \(M\)-th train. The origin of the phase relation \([38]\) may be readily understood using the Bloch sphere visualization method as illustrated in (supplemental Material at [URL will be inserted by publisher]). As the molecules slow down, the phases have to track \(v_0(t)\) as proposed in Ref. \([37]\); a typical rate of phase-tuning is \(d\Phi/dt \approx \rho_{ee}^2/(\hbar m)/N\), where \(m\) is the molecular mass. Experimentally the required phase-tuning can be attained with electro-optical modulators.

In Fig. 3(a) we investigate the time evolution of the velocity distribution for LiCl molecules. We suppose that initial cryogenic molecular beam has a \(140\) m/s forward velocity and a rotational temperature of \(\approx 1K\) \([35]\). The forward velocity distribution is modeled as a Gaussian with half-width equal to \(20\) m/s.

Initially all molecules are in the ground rovibrational manifold with \((J \leq J_{\text{max}})\) and they enter the interaction volume at the same moment of time \((t = 0)\). The laser phase follows the time evolution of \(v_0\), so the maximum of the optical force is always at \(v_0(t)\). To maximize the velocity capture range, the control phase changes as Eq. (5). The strongly peaked force (Fig. 2) leads to the compression of velocity distribution near its maximum. However since the force profile narrows with increasing number of cycles, the width of the maximum of velocity distribution starts to decrease too. The area under...
the maximum also decreases, that means that the effective number of cooled molecules grows smaller. This is caused by a build-up of destructive interferences at the wings of the force profile.

To improve the final number of decelerated molecules one could simply stop the trains and wait until all the molecules radiatively decay into the ground ro-vibrational manifold and then restart the cooling process. This would clear out all the unwanted superpositions. However the required time-scales are too long. Instead, one could employ the much faster radiative decay of the upper electronic states, Fig. 3(c). In this process additional broad-band laser pulses would drive the transitions: \( X(v, J) \to A(v', J') \), with the lower-frequency transitions \( X(v = 0, J < J_{\text{max}}) \to A(v', J') \) filtered out. Due to the spontaneous decay of the \( A(v', J') \) levels, most of the population after several absorption-radiative decay cycles gravitates towards the manifold \( X(v = 0, J < J_{\text{max}}) \) used as a starting point for stimulated cooling. We simulated such a reset/stimulated cooling scheme in Fig. 3(b). Here the stimulated cooling process is the same as in Fig. 3(a), with the addition of resetting pulses applied every 10,000 cycles. We observe that while the peak of velocity distribution becomes narrower over time, its height increases so that the area (i.e., the number of molecules) increases.

So far we neglected fine (or hyperfine) structure of molecular states. These could complicate the analysis as the pulses could couple several levels. Still one could isolate two-level transitions using chiral pulse trains. For example, for the singlet ground state diatomic molecule one could use the \( \sigma^+ (\sigma^-) \) circularly-polarized trains. Then a subset of two-level transitions \( (v = 0, J, F = I + J, M_F = I + J) \leftrightarrow (v = 1, J' = J + 1, F' = I + J + 1, M_{F'} = I + J + 1) \) becomes isolated.

FIG. 3: (Color online) Time evolution of velocity distribution of the ensemble of decelerated diatomic molecules LiCl. All molecules are initially thermally distributed over the rotational states of ground vibrational state of the ground electronic state. Initial forward velocity distribution of cryogenic molecular beam is modeled by the gaussian with center at 140 m/s and half-width equal to 20 m/s. Single pulse area \( \theta = \pi/4 \), pulse repetition period \( T = 1 \) ns. (a) Velocity distributions for the stimulated cooling scheme with Doppler phase tracking and train-to-train phase correction. (b) The same as in (a) but with additional population reset applied every 10,000 cycles.
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