Modeling cytoadhesion of *Plasmodium falciparum*-infected erythrocytes and leukocytes—common principles and distinctive features

Gesa Helms1,*, Anil Kumar Dasanna2,3,*, Ulrich S. Schwarz2,3 and Michael Lanzer1

1 Department of Infectious Diseases, Heidelberg University, Germany
2 BioQuant, Heidelberg, Germany
3 Institute for Theoretical Physics, Heidelberg University, Germany

Correspondence
M. Lanzer, Department of Infectious Diseases, Parasitology, Heidelberg University, Im Neuenheimer Feld 324, 69120 Heidelberg, Germany
Fax: +49 6221 564643
Tel: +49 6221 567845
E-mail: Michael.Lanzer@med.uni-heidelberg.de

U. Schwarz, Institute for Theoretical Physics, Heidelberg University, Philosophenweg 19, 69120 Heidelberg, Germany
Fax: +49 6221 549331
Tel: +49 6221 549431
E-mail: schwarz@thphys.uni-heidelberg.de

*These authors contributed equally.

(Received 28 December 2015, revised 1 February 2016, accepted 7 February 2016, available online 5 April 2016)

doi:10.1002/1873-3468.12142

Edited by Wilhelm Just

A drop of blood (10 μL) contains an estimated 50 million erythrocytes and approximately 5000 leukocytes, among other cells. Both red and white blood cells are easy to spot under the microscope because of their difference in color and shape. Erythrocytes are red and are shaped in the form of a biconcave discoid, whereas leukocytes are colorless and have a spherical appearance. The distinct colors and shapes are a reflection of their different biological functions. Erythrocytes are part of the respiratory and circulatory system, carrying oxygen in a complex with the red chromophore hemoglobin from the lung to the periphery of the body.

Keywords: catch bond; cytoadhesion; leukocyte; malaria; mesoscopic model; modeling
Leukocytes are cells of the immune system and are involved in controlling infections and removing foreign antigens.

Leukocytes usually move passively with the blood flow. However, in response to an inflammatory stimulus, they can roll along the microvascular endothelium and, eventually, firmly adhere (Fig. 1) [1]. Leukocytes then migrate over the endothelium until they extravasate into the surrounding tissue, where they home in on infections [2]. In comparison, erythrocytes do not adhere to the endothelial lining under normal physiological conditions. The exceptions are sickle cell erythrocytes that can adhere to postcapillary venule endothelium, a condition that is associated with vasoocclusive pain [3]. Erythrocytes stay in circulation until they are cleared by the reticuloendothelial system of the spleen and liver after an average lifetime of 120 days.

The rheological properties of erythrocytes dramatically change upon infection with the human malaria parasite *Plasmodium falciparum*. Now erythrocytes acquire adhesive properties mediated by parasite-encoded adhesins that are presented on the host cell surface in knob-like protrusions (Fig. 1) [4,5]. Strikingly, the cytoadherence of parasitized erythrocytes mimics the way leukocytes adhere (Table 1) [6]. Leukocytes are covered with hundreds of microvilli that carry adhesins such as L-selectin on their tips [1]. These adhesins interact with receptors on the surface of vascular endothelial cells, leading to cytoadhesive events that phenotypically resemble the rolling and firm adhesion displayed by *P. falciparum*-infected erythrocytes [1,6]. Thus, both infected erythrocytes and leukocytes use localized and elevated adhesive domains to adhere to vessel walls. Another similarity is the use of tension-enhanced adhesion systems [7,8]. However, in marked contrast to parasitized erythrocytes, cytoadherence of leukocytes is cooperative with the endothelium and leads to extravasation rather than sustained adhesion as is seen for *P. falciparum*-infected erythrocytes.

In this review, we discuss the similarities and differences between cytoadhesion in these two medically important cellular systems. In Cytoadhesion: a molecular perspective, we will briefly introduce the molecular players mediating cytoadhesion of *P. falciparum*-infected erythrocytes and leukocytes to endothelial cells. For a comprehensive review of the interacting receptor-ligand pairs, we refer the interested reader to specialized literature on this topic [1,5,9,10]. In Biophysics of adhesive bonds: slip or catch, we will discuss the phenomenon of tensile force-enhanced cytoadhesion. Adhesive dynamics of white blood cells and Adhesive dynamics of *P. falciparum*-infected erythrocytes will deal with the dynamic of cytoadhesion and how mathematical modeling and simulation can help us understand the mechano-physical and biophysical principles underpinning cytoadhesion in flow. In particular, we will explain the reason for placing adhesins in structures elevated above the cell surface. We close with a discussion of the similarities and differences between the two systems and an outlook on open issues that should be addressed in the future.

**Cytoadhesion: a molecular perspective**

**Pathology and cytoadhesion during a *P. falciparum* infection**

Malaria remains a leading cause of morbidity and mortality in many developing countries. According to...
the world malaria report of 2014, there were 198 million cases of malaria in 2013 and 584 000 deaths [11]. Of the five Plasmodium species that can cause malaria in humans, *P. falciparum* is the most virulent and deadly form, being responsible for most of the malaria-associated deaths. *P. falciparum* is transmitted to humans by the bite of an infected *Anopheles* mosquito. Sporozoites released into the skin enter blood vessels and are carried with the blood flow to the liver where they invade hepatocytes. An infected hepatocyte can give rise to more than 10 000 daughter cells, termed merozoites, which are released into the blood stream where they infect erythrocytes. After 48 h the infected erythrocyte bursts, releasing typically 16 or 32 merozoites that then again infect erythrocytes, thereby establishing the intraerythrocytic life cycle. In extreme cases, 40% of the approximately $2.6 \times 10^{13}$ erythrocytes of an adult malaria patient can be infected by parasites. The entire life cycle is completed when an Anopheles mosquito takes up sexual stages during a blood meal.

The asexual intraerythrocytic stages of *P. falciparum* are responsible for much of the pathology associated with malaria, whereas the liver stages are asymptomatic [12]. The virulence of the asexual blood stages is largely due to the fact that the parasite alters the rheological and morphological properties of the infected erythrocyte. Uninfected erythrocytes move in the middle of the blood vessel where the flow velocity is maximum, leaving a rim around the vessel wall free of cells [13]. This phenomenon can be explained by the Magnus effect. As soon as a cell moves out of the central part of the capillary the velocity gradient causes it to spin. The cell will then feel a force perpendicular to the flow direction and the rotational axis, which forces it back to the central region [13].

### Table 1. Comparison of cytoadhesion of leukocytes and *P. falciparum*-infected erythrocytes.

|                        | Leukocytes                                                                 | *Pf*-infected erythrocytes                     |
|------------------------|-----------------------------------------------------------------------------|------------------------------------------------|
| Adhesive structures    | 100s of microvilli, each 300 nm high                                         | 10 000s of knobs, each 20 nm high              |
| Mechanics of adhesive structure | Viscoelastic, elongates under shear flow                                    | Compact and stiff                              |
| Cell size, shape, and mechanics | Diameter 8–30 μm; spherical; flexible envelope | Diameter 6.2–8.2 μm; varies between biconcave and round, but not perfectly spherical; stiff envelope |
| Molecular system       | Mainly selectins, very specific ligands on HEV                              | PfEMP-1, broad range of receptors specific to distinct microvascular beds |
| On-set of adhesion     | Activated by chemokines, GPCR                                               | Developmentally controlled, commences 16 h post invasion until end of replicative cycle |
| Interplay with endothelium | Inside out signaling to recruit leukocytes                              | Contact-dependent intracellular signaling; clustering and activation of host adhesion receptors |
| Movement during cytoadhesion under flow conditions | Rolling on HEV                                                             | Sometimes rolling, but often irregular movement with flipping, depending on life cycle |
| Biological purpose     | Preface to extravasation                                                    | Evasion of splenic clearance                  |

GPCR, G-protein-coupled receptors; HEV, human endothelial venules; Pf, *Plasmodium falciparum*.
PfEMP1 variants encoded in the haploid *P. falciparum* genome have unique binding properties, a few PfEMP1 variants can interact with several host cell receptors, for example, CD36 and ICAM-1 [10]. Collectively, PfEMP1 proteins can interact with a broad range of receptors, including CD36, intercellular adhesion molecule 1 (ICAM 1), and P-selectin [4,5]. In addition, a certain PfEMP1 variant can mediate attachment of parasitized erythrocytes to chondroitin-4-sulfate (CSA), a component of the proteoglycan matrix present in the intervillous space and moderately on the syncytiotrophoblast cell layer of the human placenta [15–19]. Other parasite-encoded factors implicated in cytoadhesive events include the RIFINS and STEVOR immunovariant antigens that are thought to mediate rosetting of infected erythrocytes with uninfected erythrocytes [20,21].

For effective cytoadhesion, the major adhesin molecule PfEMP1 needs to be placed in parasite-induced knob-like protrusions on the erythrocyte plasma membrane (Figs 1 and 2). Knobs have a typical height of 20 nm and there can be as many as 10 000 knobs on the surface of a mature infected erythrocyte [22]. Knobs consist of several parasite and host factors. The major constituent is the knob-associated histidine-rich protein (KAHRP) [23]. This protein is encoded by the parasite and trafficked into the host erythrocyte cytoplasm. KAHRP expression is essential for cytoadhesion of parasitized erythrocytes, as demonstrated in parasite lines deficient in the kahrp gene [24]. These kahrp-deficient lines do not form knobs and the corresponding infected erythrocytes do not cytoadhere in flow, although they present PfEMP1 on the surface, suggesting that the display of PfEMP1 in knobs is critical for productive cytoadhesive interactions [24]. KAHRP contains several protein-binding domains and is known to interact with both parasite and host factors to form knobs and the cytoadhesion complex (Fig. 2). For instance, KAHRP interacts with several membrane skeletal proteins of the host erythrocyte, including spectrin, actin, ankyrin R, and spectrin–actin band 4.1 complex [25–28]. The ankyrin R and spectrin-binding domains have been mapped to amino acids 285–362 and 370–441, respectively [25,26]; the actin-binding domain is contained within residues 253–524 and most likely corresponds to the 5′ repeat unit [28,29]. KAHRP further self-aggregates possibly via the 5′ repeat unit and it can bind to the C-terminal cytoplasmic domain of PfEMP1 via one of two domains: the His-rich domain from residue 60–123 and the domain from residues 359–441 [26,28,30–32]. PfEMP1 itself is linked to the spectrin network via PHIST proteins, with members of the PHIST family interacting with PfEMP1 proteins in a variant-specific manner (Fig. 2) [33].

The interaction of both PfEMP1 and KAHRP with components of the membrane skeleton, but possibly also with parasite-induced long actin filaments (Fig. 2) [34], may provide the mechanical support for binding of PfEMP1 to endothelial surface receptors under flow conditions. Further mechanical support may be provided by a spiral structure of hitherto unknown nature, underlying the knobs [35]. The spiral structure may further contribute to the enhanced rigidity of the erythrocyte plasma membrane [35].

**Cytoadhesion of leukocytes**

Rolling adhesion of leukocytes can be seen *in vivo* as the first step toward extravasation during an acute inflammation [1,36,37]. Initial contact is established through a system of three selectin receptors: L-selectin...
is localized at the tips of the leukocyte microvilli and binds to sulfated sialyl-Lewis X-like sugars (e.g., PNAd) in high endothelial venules of the endothelium. P- and E-selectin are activated in inflamed endothelium and bind to partners, such as P-selectin glycoprotein ligand-1 (PSGL-1), which are also localized at the tips of the leukocyte microvilli (Fig. 1) [1,38]. Some integrins, such as $\alpha_4\beta_7$ and $\alpha_4\beta_1$, also contribute to rolling adhesion. One essential aspect of rolling is that it exposes the leukocytes to chemotactic signals, such as the chemokine IL-8 that then activates G-protein-coupled receptors (GPCR) [36,37]. This, in turn, leads to an inside-out activation of $\beta_2$ or $\alpha_t$-integrins that establishes firm adhesion by binding to endothelial immunoglobins. The most prominent integrins in this context are LFA-1 ($\alpha_4\beta_2$) or Mac-1 ($\alpha_{M}\beta_2$) that can bind to ICAM-1 or ICAM-2 presented on the surface of endothelial cells (Fig. 1). There are hundreds of microvilli on a leukocyte with a typical height of 300 nm. In marked contrast to the knobs on infected erythrocytes, the microvilli of leukocytes can strongly increase their length under force, due to viscoelastic flow in the membrane and the cytoskeleton [39]. Once firmly attached, the leukocytes start to migrate along the endothelium in order to induce the extravasation process that usually proceeds in cooperativity with the endothelial cells at cell–cell boundaries (paracellular route). However, there is also a second mode of extravasation, in which leukocytes simply cross endothelial cells through their cell body (transcellular route). Both processes require tight regulation of the actin cytoskeleton [40]. While rolling adhesion can be reconstituted easily in flow chambers, the study of extravasation requires more complex coculture assays or intravital microscopy.

**Biophysics of adhesive bonds: slip or catch**

Adhesive bonds are formed by noncovalent interactions between a receptor and a ligand. In a coarse-grained description, the dissociation of such noncovalent bonds can be understood from Kramers reaction rate theory. The potential minimum of such a receptor–ligand bond corresponds to the bound state, and dissociation occurs by crossing the transition-state barrier. The rate of dissociation can be written from Kramers theory as $k_{\text{off}}^0 \sim \exp(-\Delta E/k_B T)$, where $\Delta E$ represents the energy barrier height and $x_c$ is the distance between the potential minimum and the transition point. This means that the dissociation rate increases with decreasing barrier height $\Delta E$ (compare the energy landscape sketched in Fig. 3A). In 1978, George Bell formulated a model [41], which was later refined by Evans and Ritchie [42], describing the dissociation rate of molecular bonds in the presence of an external force. The application of an external force $f$ lowers the potential well to a new barrier height $\Delta E - f x_c$. Thus, the new rate of dissociation becomes $k_{\text{off}} \sim \exp(-(\Delta E - f x_c)/k_B T)$, which leads to $k_{\text{off}} = k_{\text{off}}^0 \exp(f x_c/k_B T)$. Due to the exponential relation, a small increase in force can strongly increase the dissociation rate. The bonds that become short-lived under external tensile force are called *slip bonds* [43] (Fig. 3B). This concept has been confirmed for many receptor–ligand pairs using dynamic force spectroscopy.

---

**Fig. 3.** Slip bonds versus catch bonds. (A) Energy ($E$) landscape of a noncovalent receptor–ligand bond. The bound state corresponds to a metastable minimum separated from the unbound state by a transition state barrier of height $\Delta E$. $x_c$ denotes the reactive compliance. Application of force, $f$, decreases the height of the barrier to $\Delta E - f x_c$ and therefore increases the dissociation rate. (B) As a result, the life time of the slip bond decreases when stressed by a tensile force. (C) In contrast, the lifetime of a catch-slip bond initially increases with tensile force before it decreases at higher forces.
In such experiments, the bonds are loaded by a dynamic ramp of force (which is easier to control than a constant force). From dynamic force spectroscopy measurements, the most probable rupture forces were shown to depend linearly on the logarithm of the loading rate, as expected from the Kramers–Bell–Evans model and as initially validated for biotin–streptavidin and biotin–avidin bonds [44].

Interestingly, not all receptor–ligand pairs behave as slip bonds. Some bonds are enhanced by tensile force and are referred to as catch bonds [45,46]. The concept of catch bonds was first introduced as a theoretical consideration by Dembo et al. [43] and is explained by an increase in the bond’s lifetime with increasing loading. Given that every bond slips at very high forces, a pure catch bond is not possible and one rather deals with a catch-slip bond that is long-lived at intermediate forces (Fig. 3C). Enhancement of adhesion in shear flow in the case of bacteria [47,48] and in the case of leukocytes [49] supports the possibility of catch bond behavior at the cellular level. The first direct observation of catch-slip bonds at the molecular level came from atomic force microscopic (AFM) measurements in which Marshall et al. [7] measured lifetimes of L-selectin/PSGL-1 bonds under conditions of external loading. Off-rates of L-selectin and PSGL-1 bonds were also estimated in flow chamber experiments using L-selectin-coated microspheres [50]. Off-rates were measured for two sizes of microspheres in the presence and absence of ficoll, a sugar that increases the viscosity of the medium, and, therefore, the hydrodynamic force. It was found that the catch bond behavior of L-selectin and PSGL-1 bonds is responsible for shear-enhanced adhesion. Catch bond behavior is also observed in actomyosin bonds, with increased bond lifetime with increasing loading. Given that every bond slips at very high forces, a pure catch bond is not possible and one rather deals with a catch-slip bond that is long-lived at intermediate forces (Fig. 3C).

Adhesive dynamics of white blood cells

Leukocyte rolling has been studied in vitro using flow chamber experiments where rolling of leukocytes was examined on culture dishes and artificial lipid bilayers coated with appropriate ligands. It was found that the dissociation rate of the P-selectin-glycoprotein ligand bond increases with tensile force, indicative of a slip bond, making the P-selectin–glycoprotein ligand interaction suitable for rolling adhesion [64,65]. In comparison, L-selectin-mediated adhesion involves a shear threshold, indicative of a catch bond, and only at high tensile force does the bond behave like a slip bond [50,66].

Catch bonds can be considered as hydrodynamic sensors. Like sites of trauma, sites of inflammation are characterized by vasodilation and increased shear flow. The biological purpose of catch bonds, therefore, seems to be to facilitate the adhesion of leukocytes exactly where it is needed.

Modeling adhesion of white blood cells centers around two key aspects: hydrodynamics and bond kinetics, which together are referred to as adhesive dynamics. The first to address this issue were Hammer and Apte, who took a reductionist approach by assuming that leukocytes are ideal spheres homogeneously covered with receptors and that the interacting ligands are homogenously distributed on a planar surface [67–69]. A more refined version of the model was developed by Korn and Schwarz [70] who incorporated explicit positions for receptors and ligands. The adhesion dynamics was simulated using a Langevin equation:

$$\dot{X}(t) = u^\infty + M(F_D + F_S) + k_B T \nabla M + \xi(t)$$

where $X(t)$ is a six-dimensional vector for both position and orientation. Here, the generalized force, $F$, includes both the force and the torque. The terms $F_D$ and $F_S$ are direct and shear forces, respectively. The direct forces include gravitational force and receptor–ligand bond forces. The $6 \times 6$-dimensional mobility matrix $M$ converts forces into velocities and $u^\infty$ is the unperturbed flow velocity. The stochastic random force, $\xi(t)$, represents the thermal forces from the environment, which are crucial to bring spatially resolved receptors and ligands into binding range. The spurious drift term with the spatial derivative $\nabla M$ ensures that the stochastic dynamics satisfy the requirements of equilibrium physics. In the case of a sphere in unbounded flow, the mobility matrix becomes position independent, eliminating the drift term, $\nabla M$. The ligand–receptor bond forms when the distance between
Adhesion of leukocytes and infected erythrocytes

Adhesive dynamics is able to reproduce different dynamical states, such as rolling adhesion, firm adhesion, and transient adhesion. When systematically varying the model parameters, the model allows phase diagrams to be constructed, for example, as a function of molecular association rate ($v_\text{on}$) and dissociation rate ($v_\text{off}$), one typically finds the four different regimes as shown here. Free motion is characterized by smooth changes in translational and angular velocities. At lower dissociation rates, transient adhesion occurs, with repeated binding and unbinding leading to strongly variable trajectories. Rolling is characterized by synchronization of translation and rotation and occurs for a high association rate and an intermediate dissociation rate, for example, as is seen for selectin-mediated adhesion of leukocytes. Firm adhesion with low translational and rotational velocities occurs for low dissociation rates, which corresponds to adhesion through activated integrins.

The different phases correspond to different characteristics of the individual cell trajectories. During free motion both translational and angular velocities change only in a smooth manner and no interactions occur between the cell and the substrate. Firm adhesion is achieved when the cell is firmly attached to the substrate, thus translational and rotational velocities are almost zero. During both transient and rolling adhesion, the cell moves along the substrate by constantly forming new bonds at the front end and breaking the old bonds at the rear end. This leads to strong variations in the velocities. Translation and rotation are synchronized in the case of rolling adhesion, while they are more variable and more decoupled for transient adhesion. The on–off state diagram depicted in Fig. 4 depends on many other parameters, including the receptor–ligand kinetics, the viscosity of the medium, and receptor and ligand density. For example, increases in viscosity leads to a more stable rolling at the expense of firm adhesion, leaving free motion and transient adhesion unchanged. Particularly, the receptor and ligand density strongly affects the cytoadherence efficiency [38,70]. Simulation further revealed that the binding efficiency is significantly increased if the receptors are elevated above the cell surface [70]. The physical reason is that hydrodynamic flow becomes slowed down toward the cell surface. Protrusions are, therefore, exposed to larger flows and can sample more environmental space than the cell surface. This might explain why the adhesion receptors are placed at the tip of microvilli in leukocytes and why the adhesin PfEMP1 is presented in knob-like protrusions on the surface of *P. falciparum*-infected erythrocytes. However, leukocytes with their microvilli of 300 nm in height seem to exploit this principle to a larger extent than do infected erythrocytes where knobs are only a moderate 20 nm in height. However, the large number of ten thousands of knobs as opposed to hundreds of microvilli per cell might compensate for the inferior height.

Adhesive dynamics has also been used to investigate the importance of thermal fluctuations at both low and high shear rates on adhesive behaviors [73]. Moreover, adhesive dynamics can be applied to other systems, for
example, to adhesion of tumor cells [74,75]. The model was also used to study a two receptor system [76] and catch-slip bond behavior [77], explaining the shear threshold nature of leukocyte cytoadhesion [50].

**Adhesive dynamics of *P. falciparum*-infected erythrocytes**

**Cytoadhesion in flow**

*Plasmodium falciparum*-infected erythrocytes display complex cytoadhesion phenotypes that include tumbling, rolling, and firm adhesion depending on the receptor–ligand interaction (Fig. 1). They firmly attach to CD36 and CSA, but roll over surfaces containing ICAM 1 and P-selectin at physiological wall shear stresses, as shown in flow chamber assays [78–81] (Fig. 1). Both rolling and firm adhesion can be observed in flow experiments using endothelial cells that express multiple receptors, such as ICAM1 and CD36 [80]. Li et al. [82] measured the interaction of parasitized erythrocytes with surface-coated CD36 and thrombosporin (TSP). They found that TSP initiates the cell adhesion before they firmly adhere to CD36 [82].

In a recent development, Rieger et al. [8] have studied adhesion of *P. falciparum*-infected erythrocytes to artificial membranes coated with CSA under variable hydrodynamic conditions. They found that the number of adhering cells first increases and then decreases as the wall shear stress increases. Since this behavior is reminiscent of stress-enhanced adhesion in other systems, Rieger et al. [8] proposed that the interaction between PfEMP1 and CSA behaves like a catch bond when stressed by a tensile force. Shear-enhanced adhesion is also evident for rolling adhesion of parasitized erythrocytes to ICAM-1 [78,80]. Shear-enhanced adhesion also suggests cooperative binding [8]. Whether binding of PfEMP1 variants to other host receptors is also cooperative remains to be seen.

By attaching infected erythrocyte to an AFM cantilever and then bringing them in contact with endothelial cells, Davis et al. [87] found that the adhesion force from the formation of single or multiple bonds with CD36 is initially in the range of 167 ± 208 pN. Once an initial contact is made, the adhesion force increases by five to sixfold through a signal pathway that leads to CD36 clustering and actin recruitment and polymerization at the focal point of cytoadhesion [87]. The newly formed actin filaments are thought to reinforce the interacting CD36 molecules, by anchoring them to the cytoskeleton such that they withstand the shear forces from flow [88]. Other studies have pointed out that the adhesion strength increases with parasite maturation and decreases when the temperature is raised from 37 °C to 41 °C [89,90].

The receptor density not only modulates the efficiency of cytoadherence, it is a defining factor of whether productive cytoadhesive bonds are formed in flow or not. In the case of CSA, *P. falciparum*-infected erythrocytes adhered to CSA only when the distance between neighboring CSA molecules is less than 15 nm, corresponding to 4400 CSA molecules per square micrometer [8]. This affords cytoadhesion of *P. falciparum*-infected erythrocytes in the placental intervillous space, where the CSA density is high, and not elsewhere in the microvasculature where the CSA content on endothelial cells is low—mainly confined to single CSA units attached to thrombomodulin [84].

A recent study has examined rolling of *P. falciparum*-infected erythrocytes over ICAM-1-coated surfaces as a function of the capillary size, using microfluidic devices [85]. Unexpectedly, cytoadherence was reduced in channels the size of an erythrocyte, compared to wider vessels [85]. This finding might challenge the long held view that the first capillaries to clog in vivo during a *P. falciparum* infection are the very fine microvessels.

Some studies have attempted to quantify the adhesion force between parasitized erythrocytes and endothelial cells or receptor-coated surfaces, by exposing adherent parasitized erythrocytes to gradually increasing wall shear stresses and determining the pressure (t50) at which 50% of the cells detach [78]. For cytoadherence to CSA, this value is approximately 1.3 Pa [8,81,86]. Interestingly, the wall shear stress at which 50% of the cells detach from CSA-coated surfaces depends on the receptor density in a manner that suggests cooperative binding [8]. Whether binding of PfEMP1 variants to other host receptors is also cooperative remains to be seen.
Modeling cytoadhesion of *P. falciparum*-infected erythrocytes

Modeling adhesive dynamics of infected erythrocytes requires prior knowledge of cell mechanics and the corresponding physical parameters, such as the elastic Young’s modulus. In addition, modeling requires mesoscopic models of the shape of infected erythrocytes and of the fluid flow.

The shape of an infected erythrocyte changes dramatically as the parasite matures. For the first 20 h of parasite development the host cell largely maintains its biconcave discoid shape, although a slight deformation is visible at the periphery of the host cell where the parasite resides. This quiescent phase is followed by a phase of volume increase brought about by the activation of parasite-encoded solute channels in the host cell plasma membrane [91–93]. These new permeation pathways lead to an influx of Na⁺, Cl⁻, and osmotic water. As the host cell swells due to the Na⁺-driven fluid gain, it changes its shape form a biconcave discoid to a sphere [91,94]. For characterizing these temporal changes in host cell volume, several microscopic methods have been used [95,96]. For instance, 3D models of surface-rendered views have been obtained from consecutive serial stacks of confocal fluorescence images [94], providing information regarding surface area and volume. However, only structures larger than 200 nm can be resolved by conventional microscopy. As the size of the knobs is in the range between 90 and 150 nm, with the distance between the knobs varying between 130 and 220 nm [22], standard optical microscopy is not suitable for analyzing these fine structures. Atomic force microscopy (AFM) and scanning electron microscopy (SEM) have recently provided detailed images and quantitative information regarding knob morphology and size, showing that there is a wide range of knob densities depending on the parasite strain and the type of host erythrocyte [8,22,97,98]. For instance, parasitized erythrocytes containing the sickle cell hemoglobin S or hemoglobin C (in which glutamic acid at position 6 in β-globin is substituted by valine and lysine, respectively) display abnormally enlarged and dispersed knobs [99,100]. These aberrations have been associated with the reduced cytoadherence displayed by these infected hemoglobinopathic erythrocytes [99,100]. Moreover, aberrant knob formation and impaired cytoadhesion might underpin the mechanism by which these hemoglobinopathies protect carriers from severe malaria [101,102].

As a result of the numerous parasite-induced alterations, the elastic moduli of the host plasma membrane changes during intraerythrocytic development. For instance, the parasite reorganizes the actin of the host cell, mining it from the junctional complexes of the membrane skeleton and using it to generate long actin filaments required for vesicular transport of adhesins and other virulence factors from Maurer’s clefts (unilamellar membrane profiles of parasite origin in the cytoplasm of the host cell) to the erythrocyte surface [34,103,104]. As a result of actin mining and other parasite-induced modifications of the host cell’s membrane skeleton, the original spectrin network is broken down and reorganized in the form of spectrin aggregates around the knobs, as shown by AFM imaging [98]. As a consequence of actin and spectrin remodeling and due to the generation of knobs, the erythrocyte plasma membrane becomes stiffer and less deformable [98]. Using an optical stretcher, Mauritz et al. [105] detected that the infected erythrocytes have a reduced ability to stretch as compared to uninfected erythrocytes.

![Figure 5](image-url)

**Fig. 5.** (A) Equilibrium shape of a model red blood cell generated using the mesoscopic model by Li et al. [109] for 6000 vertices. The total volume and surface area was constrained to 80 μm³ and 135 μm², respectively. (B) Triangulated lattice in which beads are connected by springs. C. Snapshots of rolling uninfected and infected erythrocytes. (i) Snapshots of rolling uninfected erythrocytes are shown. The blue dots are markers on the membrane. (ii) Snapshots of flipping infected erythrocytes (uninfected erythrocytes with high Young’s modulus) are shown. (iii) Snapshots of flipping infected erythrocytes with rigid parasite particles inside are shown. Figure reproduced from Ref [120].
Mesoscopic models for red blood cell shape

Study of adhesive dynamics in flow requires mesoscopic modeling of red blood cells. Mesoscopic or coarse-grained models of any biological system consider lower resolution subunits. One such class of mesoscopic model is a bead-spring network model where the 3D shape is represented by a triangulated network of beads connected via springs. Using this approach, the red blood cell shape has been modeled at the spectrin level (Fig. 5A,B) [106–110]. The positions of the beads or vertices are given by \( x_j \). The total surface area of an erythrocyte is the sum of areas of individual triangles, \( A_i \), and the total volume is the sum of volumes contributed by each triangle, \((\hat{n}_i \cdot x_i) A_i / 3\). The total free energy of the system is,

\[
F(\{x_j\}) = F_{\text{in-plane}} + F_{\text{bend}} + F_{\text{area}} + F_{\text{volume}}
\]

where \( F_{\text{area}} \) conserves the total surface area of the cell and \( F_{\text{volume}} \) conserves the total volume of the cell. Both \( F_{\text{area}} \) and \( F_{\text{volume}} \) are implemented as harmonic potentials about \( A_0 \) and \( V_0 \) with rigidity factors \( k_{\text{area}} \) and \( k_{\text{volume}} \), which set the strengths of the constraining potentials for surface area and volume, respectively, where \( A_0 \) and \( V_0 \) are total surface area and total volume of the cell, respectively.

The equilibrium length of the edge is \( \ell_0 \). The total bending energy is written as,

\[
F_{\text{bend}} = \sum_i \kappa_b (1 - \cos(\theta_i - \theta_0))
\]

where \( \theta_0 \) is the angle between the normals of adjacent triangles, \( \kappa_b \) is the bending constant, and \( \theta_0 \) is the spontaneous curvature angle. The bending constant, \( \kappa_b \), is related to the bending moduli of the lipid membrane, \( \kappa_r \), as \( \kappa_b = 2\sqrt{5}\kappa_r \) [108,109]. The last term in free energy \( F_{\text{in-plane}} \) is the elastic energy stored in the membrane. It is written as the sum of the elastic energy stored in spectrin links and the hydrostatic elastic energy stored in each triangle. It is written as

\[
F_{\text{in-plane}} = \sum_i V_s(\ell_i) + \sum_i \frac{C_q}{A_i}
\]

For \( V_s(\ell_i) \), there exists many nonlinear spring models such as the Worm-like Chain model (WLC) and the Finitely Extensible Non-linear Elastic (FENE) polymer model [111]. In the second term, \( C_q \) is a constant that depends on spring parameters [108,109] and \( q \) is an exponent that is chosen to be 1. The elastic moduli, such as Young’s modulus and shear modulus, can be deduced in model parameters using a linear analysis. Figure 5A shows the equilibrium shape of a model red blood cell for 5000 vertices, a total volume constrained to \( V_0 = 80 \mu m^3 \), and a total surface area of \( S_0 = 135 \mu m^2 \). The currently considered mesoscopic model contains a fixed network, meaning that it does not consider the fluid nature of lipid membranes. Noguchi and Gompper took this into account by employing dynamically triangulated lattices [112,113]. Recently, it has been shown that the surface properties of erythrocytes are also strongly determined by active elements (e.g., ion pumps) in the membrane [114].

Modeling adhesion of parasitized erythrocyte under flow

There are several coarse-grained or mesoscopic models of fluid, such as Multi Particle Collision Dynamics (MPCD) [115] and Dissipative Particle Dynamics (DPD) [116]. MPCD and DPD are off-lattice particle-based simulation techniques to model the fluid. Noguchi and Gompper [113] used MPCD for simulating the fluid along with a dynamically triangulated network model for red blood cells to study the shape transitions under capillary flow. The dynamics of solvent particles was coupled to the dynamics of membrane vertices, by including membrane vertices in solvent exchange of momentum step [117,118]. They found that model red blood cells transform from nonaxial symmetric discocyte shapes to axis symmetric parachute shapes in capillary flow and that the speed of this transition decreases with increasing elastic moduli, such as the bending modulus and the shear modulus. Fedosov et al. [108] simulated the mechanics and the dynamics of model red blood cells in flow, using the DPD method. The external solvent makes bounce-back interactions with the membrane, separating the internal and external solvent and preserving no-slip boundary conditions at the membrane. The membrane and solvent dynamics are linked via viscous force coupling.

Fedosov et al. [119,120] extended the approach to the adhesion of infected erythrocytes. Different dynamical states were recovered, such as firm adhesion, rolling adhesion, and flipping motion. Infected erythrocytes were modeled by increasing the membrane stiffness in relation to uninfected red blood cells and by placing solid particles mimicking the intracellular parasite inside the host cell cytosol. In Fig. 5C, the different adhesive behaviors of uninfected and infected erythrocytes are illustrated. Model uninfected erythrocytes change from rolling motion...
to flipping behavior when the Young’s modulus is increased three times. Irregular flipping dynamics is observed when rigid particles are placed inside the erythrocyte cytosol as models for the parasite. Thus, the transition from rolling to flipping is due to increased stiffness and the presence of an intracellular rigid parasite.

Hosseini et al. modeled infected erythrocytes at the schizont stage based on uninfected red blood cells with an internal spherical rigid parasite to simulate stretching of the cell as observed using optical tweezers [121,122]. They found that the deformability of the cell under external force decreases owing to the increased stiffness and the presence of the internal parasite.

Conclusions and perspectives

Leukocyte rolling adhesion and extravasation is a widely investigated subject in biophysics, cell biology, and immunology. In comparison, the biophysical interactions of infected red blood cells with the endothelium are much less explored in spite of the medical relevance for the pathophysiology of malaria. Table 1 provides an overview of the main differences between the two systems as discussed here. It is evident that, despite the striking similarities that might have evolved due to the physical limitations of cytoadhesion in flow, there are also marked differences that certainly matter for the biological function. Overall the leukocytes seems to be better adapted to cell capture in shear flow, as evidenced by the round shape, the mechanical design of the microvilli and the molecular properties of the different members of the selectin family. Together, these elements lead to a cascade of adhesion events that ensures efficient and specific cell capture. In direct comparison, the adhesive knobs of the infected erythrocyte, which are less elevated and stiffer than the microvilli, seem to be less efficient in this regard, possibly because the biological function does not require high effectivity or specificity. On the other hand, their large number and complex composition and architecture suggest that the situation is more complex, for example, involving interactions with the endothelium and the immune system that we do not yet fully understand.

While there has recently been substantial progress in our understanding of the cytoadherence of *P. falciparum*-infected erythrocytes in flow, there are still open questions and technical and methodological challenges to be met before this important pathological behavior of parasitized erythrocytes can be appreciated in its full complexity. From the comparison conducted in this review, it is evident that the mechanics of infected erythrocytes is crucial to a deeper insight into interactions with the endothelium. However, the mesoscopic shape model of parasitized erythrocytes needs to be improved as current models do not yet consider the effect of the knobs or temporal changes in host erythrocyte shape during the course of intracellular parasite development. In a recent development, Zhang et al. [123] have approached this gap in understanding, by calculating the shear modulus of infected erythrocytes, using a coarse-grained model where the lipid bilayer and the spectrin network were modeled separately and connected with vertical linkage. The knobs were simulated by circular areas with increased membrane stiffness and more connections with the spectrin network [123]. Such modeling advances have to be pushed further in the future as empirical data on the relevant parameters become available.

There is further a gap in our knowledge about the number of PfEMP1 molecules on the host cell surface and how many PfEMP1 molecules are present per knob. It is further not fully understood how they are displayed in knobs and with which factors they interact in these protrusions. Single-molecule counting in combination with super-resolution microscopy might help address these questions. First experiments using various super-resolution microscopic techniques [including stimulated emission microscopy (STED), photo-activated localization microscopy (PALM), stochastic optical reconstruction microscopy (STORM), and strucational illumination microscopy (SIM)] are encouraging [124–126], promising novel insights into host erythrocyte shape, knob formation, and PfEMP1 assembly and presentation in the near future. Other techniques that might help elucidate the mechanical properties of the host cell membrane include flicker microscopy, which has recently been used to study the effect of endotoxins on uninfected erythrocytes [127]. A central aspect here will be the role of passive versus active contributions to the flickering spectrum [114]. For example, it might well be that the stiffening observed for infected erythrocytes not only results from the remodeling of the spectrin network but also from changes in the cellular metabolism by the parasite. While we have first information regarding the adhesion strength at the whole cell level, the contribution of single-molecule bonds is unclear. Here, single-molecule force measurements using atomic force microscopy are anticipated to resolve this issue, following the lead in other systems [128]. Once such results are available, they can be used for adhesive dynamic simulations for cell capture from the flow.
Another pending question pertains to cytoadhesion and flow dynamics of parasitized hemoglobinopathic erythrocytes. As mentioned above carriers of the sickle cell hemoglobins S and C are protected from severe malaria (which explains why these hemoglobin polymorphisms are highly prevalent in malaria-endemic areas). Carriers are not sterile to infection. In fact, they can have parasitemias as high as those seen in patients with normal hemoglobin. However, they are less likely to develop cerebral malaria and to die from severe complications [102]. These hemoglobinopathic erythrocytes, and also fetal and \(\alpha\)-thalassemic erythrocytes (which also protect from severe malaria), possess fewer and abnormally large knobs on their surface than wild-type erythrocytes, when infected with \(P.\) \textit{falciparum} [99,100,102,129–132]. In addition, the amount of PfEMP1 molecules presented is reduced and aberrantly displayed [99,100,130]. How sickle cell hemoglobins S and C affect knob formation and cytoadherence is largely unclear as are the ramifications of the aberrant knob morphology and density for the interaction of these parasitized hemoglobinopathic erythrocytes with the microvascular endothelial lining in flow. Do they bind to endothelial cells with sufficient strength to activate the endothelium? If the adhesion strength is insufficient to trigger the life-threatening downstream inflammatory events, as recently proposed [130], then this might explain the malaria-protective trait of hemoglobinopathic and fetal erythrocytes.

Understanding cytoadhesion dynamics of leukocytes has substantially benefited from computational modeling and the application of biophysical methods and approaches. In the case of parasitized erythrocytes, this research is still at its infancy. However, progress is anticipated to accelerate given the ability of the malaria community to implement novel techniques and to learn from the experience gained in other fields.

**Acknowledgements**

This work was in part supported by the Deutsche Forschungsgemeinschaft under the Collaborative Research Center SFB 1129. USS and ML are members of the cluster of excellence CellNetworks. We thank Britta Nyboer for the art work.

**Author contributions**

USS and ML outlined the manuscript. GH, AKD, USS and ML wrote the article.

**References**

1. Simon SI and Goldsmith HL (2002) Leukocyte adhesion dynamics in shear flow. Ann Biomed Eng 30, 315–332.
2. Carman CV and Springer TA (2008) Trans-cellular migration: cell-cell contacts get intimate. Curr Opin Cell Biol 20, 533–540.
3. Hebbel RP (1991) Beyond hemoglobin polymerization: the red blood cell membrane and sickle disease pathophysiology. Blood 77, 214–237.
4. Tembo D and Montgomery J (2010) Var gene expression and human \textit{Plasmodium} pathogenesis. Future Microbiol 5, 801–815.
5. Sherman IW, Eda S and Winograd E (2003) Cytoadherence and sequestration in \textit{Plasmodium falciparum}: defining the ties that bind. Microbes Infect 5, 897–909.
6. Ho M, Hickey MJ, Murray AG, Andonegui G and Kubes P (2000) Visualization of \textit{Plasmodium falciparum}-endothelium interactions in human microvasculature: mimicry of leukocyte recruitment. J Exp Med 192, 1205–1211.
7. Marshall BT, Long M, Piper JW, Yago T, McEver RP and Zhu C (2003) Direct observation of catch bonds involving cell-adhesion molecules. Nat Rev Immunol 3, 190–193.
8. Rieger H, Yoshikawa HY, Quadri K, Nielsen MA, Sanchez CP, Salanti A, Tanaka M and Lanzer M (2015) Cytoadherence of \textit{Plasmodium falciparum}-infected erythrocytes to chondroitin-4-sulfate is cooperative and shear enhanced. Blood 125, 383–391.
9. Smith JD (2014) The role of PfEMP1 adhesion domain classification in \textit{Plasmodium falciparum} pathogenesis research. Mol Biochem Parasitol 195, 82–87.
10. Smith JD, Rowe JA, Higgins MK and Lavstsen T (2013) Malaria’s deadly grip: cytoadhesion of \textit{Plasmodium falciparum}-infected erythrocytes. Cell Microbiol 15, 1976–1983.
11. World Health Organization (2014) World Malaria Report 2014.
12. Miller LH, Baruch DI, Marsh K and Doumbo OK (2002) The pathogenic basis of malaria. Nature 415, 673–679.
13. Viallat A and Abkarian M (2014) Red blood cell: from its mechanics to its motion in shear flow. Int J Lab Hematol 36, 237–243.
14. Storm J and Craig AG (2014) Pathogenesis of cerebral malaria—inflammation and cytoadherence. Front Cell Infect Microbiol 4, 100.
15. Viebig NK, Gamain B, Scheidig C, Lepolard C, Przyborski J, Lanzer M, Gysin J and Scherf A (2005) A single member of the \textit{Plasmodium falciparum} var multigene family determines cytoadhesion to the...
placental receptor chondroitin sulphate A. *EMBO Rep* 6, 775–781.

16 Goel S and Gowda DC (2011) How specific is *Plasmodium falciparum* adherence to chondroitin 4-sulfate? Trends Parasitol 27, 375–381.

17 Fried M and Duffy PE (1996) Adherence of *Plasmodium falciparum* to chondroitin sulfate A in the human placenta. *Science* 272, 1502–1504.

18 Clausen TM, Christoffersen S, Dahlback M, Langkilde AE, Jensen KE, Resende M, Agerbaek MO, Andersen D, Berisha B, Ditlev SB et al. (2012) Structural and functional insight into how the *Plasmodium falciparum* VAR2CSA protein mediates binding to chondroitin sulfate A in placental malaria. *J Biol Chem* 287, 23332–23345.

19 Srivastava A, Gangnard S, Round A, Dechavanne S, Juillerat A, Raynal B, Faure G, Baron B, Ramboarina et al. (2014) STEVOR is a *Plasmodium falciparum* erythrocyte binding protein that mediates merozoite invasion and rosetting. *Cell Host Microbe* 16, 81–93.

20 Goel S, Pulnkivist M, Moll K, Joannin N, Lara P, Akhouri RR, Moradi N, Ojemalm K, Westman M, Angeletti D et al. (2015) RIFINs are adhesins implicated in severe *Plasmodium falciparum* malaria. *Nat Med* 21, 314–317.

21 Quadt KA, Barford L, Andersen D, Bruun J, Gyan B, Hassenkam T, Ofori MF and Hvid L (2012) The density of knobs on *Plasmodium falciparum*-infected erythrocytes depends on developmental age and varies among isolates. *PLoS One* 7, e45658.

22 Pologe LG, Pavlovcev A, Shio H and Ravetch JV (1987) Primary structure and subcellular localization of the knob-associated histidine-rich protein of *Plasmodium falciparum*. *Proc Natl Acad Sci USA* 84, 7139–7143.

23 Crabb BS, Cooke BM, Reeder JC, Waller RF, Caruana SR, Davern KM, Wickham ME, Brown GV, Coppel RL and Cowman AF (1997) Targeted gene disruption shows that knobs enable malaria-infected red cells to cytoadhere under physiological shear stress. *Cell* 89, 287–296.

24 Weng H, Guo X, Papoin J, Wang J, Coppel R, Mohandas N and An X (2014) Interaction of *Plasmodium falciparum* knob-associated histidine-rich protein (KAHRP) with erythrocyte ankyrin R is required for its attachment to the erythrocyte membrane. *Biochim Biophys Acta* 1838, 185–192.

25 Pei X, An X, Guo X, Tarnawski M, Coppel R and Mohandas N (2005) Structural and functional studies of interaction between *Plasmodium falciparum* knob-associated histidine-rich protein (KAHRP) and erythrocyte spectrin. *J Biol Chem* 280, 31166–31171.

26 Oh SS, Voigt S, Fisher D, Yi SJ, LeRoy PJ, Derick LH, Liu S and Chishti AH (2000) *Plasmodium falciparum* erythrocyte membrane protein 1 is anchored to the actin-spectrin junction and knob-associated histidine-rich protein in the erythrocyte skeleton. *Mol Biochem Parasitol* 108, 237–247.

27 Kilejian A, Rashid MA, Aikawa M, Aji T and Yang YF (1991) Selective association of a fragment of the knob protein with spectrin, actin and the red cell membrane. *Mol Biochem Parasitol* 44, 175–181.

28 Rug M, Prescott SW, Fernandez KM, Cooke BM and Cowman AF (2006) The role of KAHRP domains in knob formation and cytoadherence of *P. falciparum*-infected human erythrocytes. *Blood* 108, 370–378.

29 Moegowen C, Nunomura W, Waller KL, Yeung J, Liang J, Van Dort H, Low PS, Coppel RL and Mohandas N (2000) *Plasmodium falciparum* histidine-rich protein 1 associates with the band 3 binding domain of ankyrin in the infected red cell membrane. *Biochim Biophys Acta* 1502, 461–470.

30 Ganguly AK, Ranjan P, Kumar A and Bhavesh NS (2015) Dynamic association of PfEMP1 and KAHRP in knobs mediate cytoadherence during *Plasmodium* invasion. *Sci Rep* 5, 8617.

31 Waller KL, Cooke BM, Nunomura W, Mohandas N and Coppel RL (1999) Mapping the binding domains involved in the interaction between the *Plasmodium falciparum* knob-associated histidine-rich protein (KAHRP) and the cytoadherence ligand *P. falciparum* erythrocyte membrane protein 1 (PfEMP1). *J Biol Chem* 274, 23808–23813.

32 Oberli A, Slater L, Cutts E, Brand F, Mundwiler-Puchlatko E, Rusch S, Masik MF, Erat MC, Beck HP and Vakonakis I (2014) A *Plasmodium falciparum* PHIST protein binds the virulence factor PfEMP1 and comigrates to knobs on the host cell surface. *FASEB J* 28, 4420–4433.

33 Cyrliff M, Sanchez CP, Kilian N, Bisseye C, Simpore J, Frischknecht F and Lanzer M (2011) Hemoglobins S and C interfere with actin remodeling in *Plasmodium falciparum*-infected erythrocytes. *Science* 334, 1283–1286.

34 Watermeyer JM, Hale VL, Hackett F, Clare DK, Cutts EE, Vakonakis I, Fleck RA, Blackman MJ and Saibil HR (2016) A spiral scaffold underlies cytoadherent knobs in *Plasmodium falciparum*-infected erythrocytes. *Blood*, 127, 343–351.

35 Springer TA (1994) Traffic signals for lymphocyte recirculation and leukocyte emigration: the multistep paradigm. *Cell* 76, 301–314.
Luster AD, Alon R and von Andrian UH (2005) Immune cell migration in inflammation: present and future therapeutic targets. Nat Immunol 6, 1182–1190.

Sunid P, Pospieszalska MK, Cheung LS, Konstantopoulos K and Ley K (2011) Biomechanics of leukocyte rolling. Biorehology 48, 1–35.

Shao JY, Ting-Beall HP and Hochmuth RM (1998) Static and dynamic lengths of neutrophil microvilli. Proc Natl Acad Sci USA 95, 6797–6802.

Heasman SJ and Ridley AJ (2010) Multiple roles for RhoA during T cell transendothelial migration. Small GTPases 1, 174–179.

Bell GI (1978) Models for the specific adhesion of cells to cells. Science 200, 618–627.

Evans E and Ritchie K (1997) Dynamic strength of molecular adhesion bonds. Biophys J 72, 1541–1555.

Dembo M, Torney DC, Saxman K and Hammer D (1988) The reaction-limited kinetics of membrane-to-surface adhesion and detachment. Proc R Soc Lond B Biol Sci 234, 55–83.

Merkel R, Nasso P, Leung A, Ritchie K and Evans E (1999) Energy landscapes of receptor-ligand bonds explored with dynamic force spectroscopy. Nature 397, 50–53.

Zhu C, Lou J and McEver RP (2005) Catch bonds: physical models, structural bases, biological function and rheological relevance. Biochemistry 42, 443–462.

Chakrabarti S, Hinzewski M and Thirumalai D (2016) Phenomenological and microscopic theories for catch bonds. arXiv:1601.02050 [q-bio.BM].

Thomas WE, Nilsson LM, Forero M, Sokurenko EV and Vogel V (2004) Shear-dependent ‘stick-and-roll’ adhesion of type 1 fimbriated Escherichia coli. Mol Microbiol 53, 1545–1557.

Nilsson LM, Thomas WE, Trintchina E, Vogel V and Sokurenko EV (2006) Catch bond-mediated adhesion without a shear threshold: trimannose versus monomannose interactions with the FimH adhesin of Escherichia coli. J Biol Chem 281, 16656–16663.

Finger EB, Puri KD, Alon R, Lawrence MB, von Andrian UH and Springer TA (1996) Adhesion through L-selectin requires a threshold hydrodynamic shear. Nature 379, 266–269.

Yago T, Wu J, Wey CD, Klopopki AG, Zhu C and McEver RP (2004) Catch bonds govern adhesion through L-selectin at threshold shear. J Cell Biol 166, 913–923.

Guo B and Guilford WH (2006) Mechanics of actomyosin bonds in different nucleotide states are tuned to muscle contraction. Proc Natl Acad Sci USA 103, 9844–9849.

Thomas WE, Trintchina E, Forero M, Vogel V and Sokurenko EV (2002) Bacterial adhesion to target cells enhanced by shear force. Cell 109, 913–923.
facilitating fast rebinding events. Proc Natl Acad Sci USA 101, 6940–6945.
67 Caputo KE and Hammer DA (2005) Effect of microvillus deformability on leukocyte adhesion explored using adhesive dynamics simulations. Biophys J 89, 187–200.
68 Chang KC, Tees DF and Hammer DA (2000) The state diagram for cell adhesion under flow: leukocyte rolling and firm adhesion. Proc Natl Acad Sci USA 97, 11262–11267.
69 Hammer DA and Apte SM (1992) Simulation of cell rolling and adhesion on surfaces in shear flow: general results and analysis of selectin-mediated neutrophil adhesion. Biophys J 63, 35–57.
70 Korn C and Schwarz US (2006) Efficiency of initiating cell adhesion in hydrodynamic flow. Phys Rev Lett 93, 138103.
71 Alon R, Chen S, Puri KD, Finger EB and Springer TA (1997) The kinetics of L-selectin tethers and the mechanics of selectin-mediated rolling. J Cell Biol 138, 1169–1180.
72 Korn CB and Schwarz US (2008) Dynamic states of cells adhering in shear flow: from slipping to rolling. Phys Rev E Stat Nonlin Soft Matter Phys 77, 041904.
73 Ramesh KV, Thaokar R, Prakash JR and Prabhakar R (2015) Significance of thermal fluctuations and hydrodynamic interactions in receptor-ligand-mediated adhesive dynamics of a spherical particle in wall-bound shear flow. Phys Rev E Stat Nonlin Soft Matter Phys 91, 022302.
74 Cheung LS-L, Zheng X, Wang L, Baygents JC, Guzman R, Schroeder JA, Heimark RL and Zohar Y (2011) Adhesion dynamics of circulating tumor cells under shear flow in a bio-functionalized microchannel. J Micromech Microeng 21, 054033.
75 Zheng X, Cheung LS, Schroeder JA, Jiang L and Zohar Y (2011) Cell receptor and surface ligand density effects on dynamic states of adhering circulating tumor cells. Lab Chip 11, 3431–3439.
76 Bhatia SK, King MR and Hammer DA (2003) The state diagram for cell adhesion mediated by two receptors. Biophys J 84, 2671–2690.
77 Caputo KE, Lee D, King MR and Hammer DA (2007) Adhesive dynamics simulations of the shear threshold effect for leukocytes. Biophys J 92, 787–797.
78 Nash GB, Cooke BM, Marsh K, Berendt A, Newbold C and Stuart J (1992) Rheological analysis of the adhesive interactions of red blood cells parasitized by Plasmodium falciparum. Blood 79, 798–807.
79 Cooke BM, Berendt AR, Craig AG, MacGregor J, Newbold CI and Nash GB (1994) Rolling and stationary cytoadheson of red blood cells parasitized by Plasmodium falciparum: separate roles for ICAM-1, CD36 and thrombospondin. Br J Haematol 87, 162–170.
80 Yipp BG, Anand S, Schollaardt T, Patil KD, Looareesuwan S and Ho M (2000) Synergism of multiple adhesion molecules in mediating cytoadherence of Plasmodium falciparum-infected erythrocytes to microvascular endothelial cells under flow. Blood 96, 2292–2298.
81 Cooke BM, Rogerson SJ, Brown GV and Coppel RL (1996) Adhesion of malaria-infected red blood cells to chondroitin sulfate A under flow conditions. Blood 88, 4040–4044.
82 Li A, Lim TS, Shi H, Yin J, Tan SJ, Li Z, Low BC, Tan KS and Lim CT (2011) Molecular mechanistic insights into the endothelial receptor mediated cytoadherence of Plasmodium falciparum-infected erythrocytes. PLoS One 6, e16929.
83 Duffy PE (2007) Plasmodium in the placenta: parasites, parity, protection, prevention and possibly preeclampsia. Parasitology 134, 1877–1881.
84 Martin FA, Murphy RP and Cummins PM (2013) Thrombomodulin and the vascular endothelium: insights into functional, regulatory, and therapeutic aspects. Am J Physiol Heart Circ Physiol 304, H1585–H1597.
85 Antia M, Herricks T and Rathod PK (2007) Microfluidic modeling of cell-cell interactions in malaria pathogenesis. PLoS Pathog 3, e99.
86 Avril M, Traore B, Costa FT, Lepolard C and Gysin J (2004) Placenta cryosections for study of the adhesion of Plasmodium falciparum-infected erythrocytes to chondroitin sulfate A in flow conditions. Microbes Infect 6, 249–255.
87 Davis SP, Amrein M, Gillrie MR, Lee K, Muruve DA and Ho M (2012) Plasmodium falciparum-induced CD36 clustering rapidly strengthens cytoadherence via p130CAS-mediated actin cytoskeletal rearrangement. FASEB J 26, 1119–1130.
88 Davis SP, Lee K, Gillrie MR, Roa L, Amrein M and Ho M (2013) CD36 recruits alpha(5)beta(1) integrin to promote cytoadherence of P. falciparum-infected erythrocytes. PLoS Pathog 9, e1003590.
89 Xu X, Efremov AK, Li A, Lai L, Dao M, Lim CT and Cao J (2013) Probing the cytoadherence of malaria infected red blood cells under flow. PLoS One 8, e64763.
90 Carvalho PA, Diez-Silva M, Chen H, Dao M and Suresh S (2013) Cytoadherence of erythrocytes invaded by Plasmodium falciparum: quantitative contact-probing of a human malaria receptor. Acta Biomater 9, 6349–6359.
91 Mauritz JM, Esposito A, Ginsburg H, Kaminski CF, Tiffert T and Lew VL (2009) The homeostasis of Plasmodium falciparum-infected red blood cells. PLoS Comput Biol 5, e1000339.
Desai SA (2012) Ion and nutrient uptake by malaria parasite-infected erythrocytes. *Cell Microbiol* 14, 1003–1009.

Lew VL, Tiffert T and Ginsburg H (2003) Excess hemoglobin digestion and the osmotic stability of *Plasmodium falciparum*-infected red blood cells. *Blood* 101, 4189–4194.

Esposito A, Choimet JB, Skepper JN, Mauritz JM, Lew VL, Kaminski CF and Tiffert T (2010) Quantitative imaging of human red blood cells infected with *Plasmodium falciparum*. *Biophys J* 99, 953–960.

Cho S, Kim S, Kim Y and Park Y (2012) Optical imaging techniques for the study of malaria. *Trends Biotechnol* 30, 71–79.

Mauritz JM, Esposito A, Tiffert T, Skepper JN, Warley A, Yoon YZ, Ciuta P, Lew VL, Guck JR and Kaminski CF (2010) Biophotonic techniques for the study of malaria-infected red blood cells. *Med Biol Eng Comput* 48, 1055–1063.

Subramani R, Quadt K, Jeppeus AE, Hempel C, Petersen JE, Hassenkam T, Hvid L and Barford L (2015) *Plasmodium falciparum*-infected erythrocyte knob density is linked to the PfEMP1 variant expressed. *MBio* 6, e01456–15.

Shi H, Liu Z, Li A, Yin J, Chong AG, Tan KS, Zhang Y and Lim CT (2013) Impaired cytoskeletal modifications in *Plasmodium falciparum*-infected erythrocytes containing sickle hemoglobin. *Proc Natl Acad Sci USA* 105, 991–996.

Fairhurst RM, Baruch DI, Brittain NJ, Ostera GR, Wallach JS, Hoang HL, Hayton K, Guindo A, Makobongo MO, Schwartz OM et al. (2005) Abnormal display of PIEMP-1 on erythrocytes carrying haemoglobin C may protect against malaria. *Nature* 435, 1117–1121.

Taylor SM, Cerami C and Fairhurst RM (2013) Hemoglobinopathies: slicing the Gordian knot of *Plasmodium falciparum* malaria pathogenesis. *PLoS Pathog* 9, e1003327.

Taylor SM, Parobek CM and Fairhurst RM (2012) Haemoglobinopathies and the clinical epidemiology of malaria: a systematic review and meta-analysis. *Lancet Infect Dis* 12, 457–468.

Cyrklaff M, Sanchez CP, Frischknecht F and Lanzer M (2012) Host actin remodeling and protection from malaria by hemoglobinopathies. *Trends Parasitol* 28, 479–485.

Kilian N, Dittmer M, Cyrklaff M, Ouermi D, Bisseye C, Simpore J, Frischknecht F, Sanchez CP and Lanzer M (2013) Haemoglobin S and C affect the motion of Maurer’s clefts in *Plasmodium falciparum*-infected erythrocytes. *Cell Microbiol* 15, 1111–1126.

Mauritz JM, Tiffert T, See R, Lautenschlager F, Esposito A, Lew VL, Guck J and Kaminski CF (2010) Detection of *Plasmodium falciparum*-infected red blood cells by optical stretching. *J Biomed Opt* 15, 030517.

Boey SK, Boal DH and Discher DE (1998) Simulations of the erythrocyte cytoskeleton at large deformation. I. Microscopic models. *Biophys J* 75, 1573–1583.

Discher DE, Boal DH and Boey SK (1998) Simulations of the erythrocyte cytoskeleton at large deformation. II. Micropipette aspiration. *Biophys J* 75, 1584–1597.

Fedosov DA, Caswell B and Karmiadakis GE (2010) A multiscale red blood cell model with accurate mechanics, rheology, and dynamics. *Biophys J* 98, 2215–2225.

Li J, Dao M, Lim CT and Suresh S (2005) Spectrin-level modeling of the cytoskeleton and optical tweezers stretching of the erythrocyte. *Biophys J* 88, 3707–3719.

Pivkin IV and Karmiadakis GE (2008) Accurate coarse-grained modeling of red blood cells. *Phys Rev Lett* 101, 118105.

Marko JF and Sigia ED (1995) Stretching DNA. *Macromolecules* 28, 8759–8770.

Gompper G and Kroll DM (1997) Network models of fluid, hexatic and polymerized membranes. *J Phys Condens Matter* 9, 8795–8834.

Noguchi H and Gompper G (2005) Shape transitions of fluid vesicles and red blood cells in capillary flows. *Proc Natl Acad Sci USA* 102, 14159–14164.

Turler H, Fedosov DA, Audoly B, Auth T, Gov NS, Sykes C, Joanny J-F, Gompper G and Betz T (2016) Equilibrium physics breakdown reveals the active nature of red blood cell flickering. *Nat Phys*, doi:10.1038/nphys3621.

Malevanets A and Kapral R (1999) Mesoscopic model for solvent dynamics. *J Chem Phys* 110, 8605–8613.

Hoogerbrugge PJ and Koelman JMVA (1992) Simulating microscopic hydrodynamic phenomena with dissipative particle dynamics. *Europhys Lett* 19, 155–190.

Kikuchi N, Pooley CM, Ryder JF and Yeomans JM (2011) Quantifying the biophysical characteristics of parasite-infected red blood cells in microcirculation. *Proc Natl Acad Sci USA* 108, 35–39.
Fedosov DA, Caswell B and Karniadakis GE (2011) Wall shear stress-based model for adhesive dynamics of red blood cells in malaria. *Biophys J* **100**, 2084–2093.

Dao M, Lim CT and Suresh S (2003) Mechanics of the human red blood cell deformed by optical tweezers. *J Mech Phys Solids* **51**, 2259–2280.

Hosseini SM and Feng JJ (2012) How malaria parasites reduce the deformability of infected red blood cells. *Biophys J* **103**, 1–10.

Zhang Y, Huang C, Kim S, Golkaram M, Dixon MW, Tilley L, Li J, Zhang S and Suresh S (2015) Multiple stiffening effects of nanoscale knobs on human red blood cells infected with *Plasmodium falciparum* malaria parasite. *Proc Natl Acad Sci USA* **112**, 6068–6073.

Hans N, Relan U, Dubey N, Gaur D and Chauhan VS (2015) Identification and localization of a Novel Invasin of *Plasmodium falciparum*. *Mol Biochem Parasitol* **202**, 38–43.

Hliscs M, Millet C, Dixon MW, Siden-Kiamos I, McMillan P and Tilley L (2015) Organization and function of an actin cytoskeleton in *Plasmodium falciparum* gametocytes. *Cell Microbiol* **17**, 207–225.

Riglar DT, Richard D, Wilson DW, Boyle MJ, Dekiwadia C, Turnbull L, Angrisano F, Marapana DS, Rogers KL, Whitchurch CB *et al.* (2011) Super-resolution dissection of coordinated events during malaria parasite invasion of the human erythrocyte. *Cell Host Microbe* **9**, 9–20.

Ito H, Kuss N, Rapp BE, Ichikawa M, Gutmans T, Brandenburg K, Poschl JM and Tanaka M (2015) Quantification of the influence of endotoxins on the mechanics of adult and neonatal red blood cells. *J Phys Chem B* **119**, 7837–7845.

Wijeratne SS, Martinez JR, Grindel BJ, Frey EW, Li J, Wang L, Farach-Carson MC and Kiang CH (2016) Single molecule force measurements of perlecan/HSPG2: a key component of the osteocyte pericellular matrix. *Matrix Biol* **50**, 27–38.

Amaratunga C, Lopera-Mesa TM, Brittain NJ, Cholera R, Arie T, Fujioka H, Keefer JR and Fairhurst RM (2011) A role for fetal hemoglobin and maternal immune IgG in infant resistance to *Plasmodium falciparum* malaria. *PLoS One* **6**, e14798.

Fairhurst RM, Bess CD and Krause MA (2012) Abnormal PfEMP1/knob display on *Plasmodium falciparum*-infected erythrocytes containing hemoglobin variants: fresh insights into malaria pathogenesis and protection. *Microbes Infect* **14**, 851–862.

Fairhurst RM, Fujioka H, Hayton K, Collins KF and Wellem TE (2003) Aberrant development of *Plasmodium falciparum* in hemoglobin CC red cells: implications for the malaria protective effect of the homozygous state. *Blood* **101**, 3309–3315.

Krause MA, Diakite SA, Lopera-Mesa TM, Amaratunga C, Arie T, Traore K, Doumbia S, Konate D, Keefer JR, Diakite M *et al.* (2012) alpha-Thalassemia Impairs the cytoadherence of *Plasmodium falciparum*-infected erythrocytes. *PLoS One* **7**, e37214.