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Influence of Air Cooling Jets on the Steady-State Shape of Strips in Hot Dip Galvanizing Lines

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Abstract: The influence of air cooling jets on the steady-state shape of the strip in hot dip galvanizing lines is investigated. For this purpose, the force characteristic of a single nozzle is measured by a laboratory flow simulator. This approach differs from conventional methods, where typically, CFD simulations are used. Based on the air cooler force characteristic the stability of the equilibrium points is investigated and the influence of different types of boundary conditions, tensile loads, strip thicknesses, and cooler fan speeds is examined.

Keywords: Mechanical system, Static models, Moving objects, Distributed-parameter system, Mathematical model, Stability analysis, Steel industry, Numerical simulation, Equilibrium.

1. INTRODUCTION

In hot dip galvanizing lines, like the one shown in Fig. 1, cold-rolled steel strip is coated in a bath of molten zinc. The strip is heated in an annealing furnace and guided by the sink roll. It leaves the zinc bath after passing both the correction and stabilization roll. Above the zinc pool, gas wiping dies are mounted across the width of the strip to reduce the thickness of the zinc layer to a certain value. Cooling arrays consisting of four cooling sections are located at the upper part of the galvanizing line. They guarantee a solidified zinc layer once the strip reaches the tower roll.

Experience over many years has shown that cooling jets can influence the stability of the strip motion, in particular when thinner and broader strips are processed. Moreover, in special cases even unwanted vibrations of the strip may be induced or the strip may collide with the nozzles of the cooling section. Many studies on the modeling of axially moving beams and membranes are available (Shin et al., 2006; Steinboeck et al., 2015; Pellicano and Vestroni, 2000; Antman, 2006; Chen, 2005; Marynowski and Kapitaniak, 2014), but up to the authors’ knowledge no systematic investigations of the influence of the cooling array air jets on the stability of the strip in hot dip galvanizing lines can be found in the literature. The effect of the air cooling jets on the shape and on the stability of the strip is investigated in this paper.

For this, three eddy current sensors were used to examine the interaction between the cooler fan speed and the relative displacement of the strip. Two displacement sensors were assembled between the cooling sections 3 and 4 in order to measure the displacement at the outer edges of the strip: One at the drive side (DS), the other one at the operator side (OS). The third sensor was located in the middle of the strip (MI). The fan speed $n_2$ of cooler 2 was...
varied, all other fan speeds \( n_1, n_3 \) and \( n_4 \) and the most important parameters of the plant were held constant for this experiment. Fig. 2 shows the measured relationship between the fan speed \( n_2 \) and the displacement \( \Delta d \) of the strip for both increasing and decreasing fan speeds. The displacement \( \Delta d \) of each sensor is measured relative to its starting position. Displacements \( \Delta d \) for increasing fan speeds (up) are shown with bold lines and decreasing fan speeds are designated with thin lines. The fan speed was kept constant at a certain level for a few seconds and for this time interval the displacement measurements were averaged. The averaged data points are highlighted with markers. These measurement results clearly show that the strip displacement is influenced by the fan speed setting, although the absolute position of the strip is unknown. Ad-

\[
\Delta d = c_1 n + c_2 n^2 \quad (1)
\]

are determined as \( c_1 = 1.6785 \times 10^{-4} \text{ mbar min} \) and \( c_2 = 1.1847 \times 10^{-5} \text{ mbar min}^2 \). In order to study the pressure-force of an impinging nozzle jet on the strip a flow simulator was developed.

2. FLOW SIMULATOR

A cooling section with the parameters in Table 1 is outlined in Fig. 3. All pipes are supplied by an air blower from the DS. With negligible pressure drop inside the pipes of one section, the air stream through all nozzles must be the same. Furthermore, the flow conditions after the fluid leaves the nozzle are similar. This assumption is supported by the geometry of the cooling section, where the fluid can only escape to the rear side. For a proper analysis of the force characteristic, a laboratory flow simulator with three nozzles was setup. The mechanism of an impinging jet force on a plate was analyzed for various distances \( h_s \) between the nozzle and the plate/strip and various relative pipe pressures \( p \). Several design aspects have been taken into account. First of all, the force application surface is in line with the associated area of the strip at the real cooling panel. Also, the diameter of the pipe is equal to the real cooling pipe and the lateral distance between neighboring nozzles is the same as in the real system. The vertical distance \( l_p \) between the single pipes equals the depth of the simulator. Thus the channel for the back-flow is also identical to the real cooling section. In order to account for the stream interactions between neighboring nozzles, at least three nozzles were used. Friction alongside the simulator wall can be neglected as a result of low fluid velocity at the wall. The flow simulator is shown in Fig. 4.

Fig. 5 shows the measured force \( F_s \) acting on the area \( A_s \) as a function of the pressure \( p \) depending on the distance \( h_s \). An interesting feature can be seen in Fig. 6: In normal operating situations (\( h_s > 1 \text{ cm} \)), there is no influence of the distance \( h_s \) on the flow rate \( V_s \) of air. During the measurements, \( h_s \) was varied from 0 to \( l_w \).

| Parameter | Value | Unit |
|-----------|-------|------|
| \( d_p \) | 168.3 | mm   |
| \( l_p \) | 250   | mm   |
| \( l_w \) | 110   | mm   |
| \( l_w \) | 250   | mm   |
| \( d_n \) | 17.5  | mm   |

Table 1. Parameters of cooling section.
3. MODEL OF AXIALLY MOVING STRIP WITH COOLING PANELS

3.1 Cooling Sections

To transfer the results of the simulator to the nozzles of the plant, an offset displacement \( w = h_s - l_w/2 \) must be introduced, see Figs. 4 and 3 for details. Based on the results obtained so far, in particular Fig. 5, a semi-empirical relation of the form

\[
F_s (p, w) = (p + c_3 p^3) (c_4 e^{-c_5 w} + c_6 w + c_7)
\]  

(2)

is derived, with the parameters \( c_3, c_4, c_5, c_6, \) and \( c_7 \) according to Table 2, see Fig. 7. For a nozzle pair consisting of two vis-à-vis nozzles, the resulting pressure load on the area \( A_s \) is then derived as

\[
q_c (p, w) = \frac{F_s (p, w + w_0) - F_s (p, -w - w_0)}{A_s}.
\]  

(3)

Here, \( w_0 \) is a constant transversal offset displacement of the strip. See Fig 8 for more details. It is assumed that all nozzle pairs over the whole width of the strip exert the same force on the strip.

---

**Table 2. Parameters of impinging jet force characteristic.**

| Parameter | Value  | Unit |
|-----------|--------|------|
| \( c_3 \) | \(-2.8969 \times 10^{-5}\) | \(1/Pa\) |
| \( c_4 \) | \(-1.6449 \times 10^{-6}\) | \(m^2\) |
| \( c_5 \) | 43.9435 | \(1/m\) |
| \( c_6 \) | 4.0861 \times 10^{-4} | \(m\) |
| \( c_7 \) | 2.1788 \times 10^{-4} | \(m^2\) |
with the boundary conditions at the bottom edge
\[ u(0) = 0 \] (5)
and at the upper edge
\[ N_{xx}(L) = N_{xx} \] (6)
for a strip with prescribed tensile load (boundary condition A) or
\[ u(L) = \dot{u}_L = \frac{L N_{xx}}{EA} \] (7)
for a geometrical boundary condition, where the strip is preloaded with the force $N_{xx}$ and then fixed (boundary condition B), see Fig. 8. In (4), $N_{xx}$ is referred to as the tensile force (also denoted as membrane force). The strip velocity $V$ is assumed to be constant, and $w_0$ is a displacement offset of the strip in $z$-direction. The Euler-Lagrange equation for the steady-state displacement $w$ in $z$-direction (out-of-plane displacement) takes the form (Shin et al., 2006; Reddy, 2006)

\[ \rho AV^2 \frac{\partial^2 w}{\partial t^2} - M_{xx}' - (N_{xx} w')' - q = 0, \] (8)

with equal boundary conditions at the bottom and the upper edge. They can be written as

\[ w(0) = w(L) = w_0 \quad \text{and} \quad M_{xx}(0) = M_{xx}(L) = 0. \] (9)

Rotation with respect to the $y$-axis is free. In (8), $M_{xx}$ represents the bending moment. With $q$ as a transversal load acting on the strip, the pressure load $q_b$ induced by the cooler sections can be considered according to (3). Furthermore, $\rho$ is the mass density and $A$ the cross sectional area of the strip. Thus $\rho A$ denotes the mass density per unit length of the strip. The expression $\rho AV^2 w''$ represents the centrifugal force.

With the geometrically nonlinear strain relation $\epsilon$ and the curvature $\kappa$ of the strip,

\[ \epsilon(x) = u' + \frac{1}{2}(u')^2 \quad \text{and} \quad \kappa(x) = w'', \] (10)

the stress resultants for free transversal contraction can be written as

\[ N_{xx}(x) = EA \epsilon \quad \text{and} \quad M_{xx}(x) = -\frac{Ebh^3}{12} \kappa, \] (11)

with Young’s modulus $E$, the strip width $b$ and the strip thickness $h$. Due to (10), transversal and longitudinal displacements are coupled.

3.3 Stability of Equilibrium Points

For the proof of asymptotic stability, a dynamic model of the strip is required. In order to do so, (8) was extended to a dynamic model as given in (Shin et al., 2006; Reddy, 2006; Steinboeck et al., 2015)

\[ \rho A \left( \ddot{w} + 2V \dot{w} + V^2 w' \right) - M_{xx}' - (N_{xx} w')' - q + c_w \dot{w} = 0, \] (12)

with the additional expressions $\rho A \ddot{w}$ as the acceleration force, $\rho AV^2 \dot{w}'$ as the Coriolis force and $c_w \dot{w}$ is a linear damping force. Due to the assumption of small amplitudes, high frequencies and fast decaying in-plane vibrations, the in-plane dynamics was neglected. This assumption leads to a quasi-static relationship at every time step between the boundary condition (6) or (7), the $w$- and the $u$-displacement field.

4. NUMERICAL RESULTS

The problem that has to be solved consists of the partial differential equations (4) and (8) and the related boundary conditions (5), (6) or (7) and (9). For a numerical solution of the problem (4) and (8), a spatial discretization of the model is necessary. In longitudinal direction, the strip is divided into finite elements of equal length. For each element, the Galerkin weighted residual method is used for both in-plane and out-of-plane motion. As trial functions, Hermite polynomials are employed. They can be easily adapted to the different boundary conditions A and B of the strip. Before solving the algebraic equations gained from the Galerkin method, it is useful to normalize all Galerkin coefficients. The normalized nonlinear system is then solved with the Newton-Raphson method in combination with a line search method as described by Shearer and Cesnik (2006).

For all simulations, the parameter values were chosen as follows: The length of the strip $L = 56.5 \text{ m}$ is discretized with 60 elements, the width is $b = 1.65 \text{ m}$, and a constant strip velocity $V = 105 \text{ mm/s}$ is assumed. The material parameters of the strip are the mass density $\rho = 7850 \text{ kg/m}^3$ and Young’s modulus $E = 1.8 \times 10^4 \text{ N/m}^2$. The geometry of the cooling array is defined by $L_0 = 34.1025 \text{ m}$, $L_b = 5.205 \text{ m}$ and $L_c = 5 \text{ m}$. The damping factor $c_w$ (only used for the investigations of the stability of the equilibrium) is assumed to be $16.5 \text{ Ns/m}^2$. Parameters like strip thickness $h$, tensile resp. prestress load $N_{xx}$, pressure $p$ of the cooler pipe and the offset $w_0$ may vary from simulation to simulation.

For simplification, all cooling sections are held on equal pressure level for every simulation. Simulations without an offset yield solutions that are symmetrical with respect to the $x$-axis. Therefore, only the solution for one side (one sign of $w$) is visualized in the following. Furthermore, a more general representation is obtained using the specific load $N_{xx}/b$.

4.1 Types of Equilibria

For the proof of asymptotic stability, an early lumping approach was used. After the spatial discretization with the Galerkin method, the ordinary differential equation and the algebraic equation gained from (12) and (4) can be written as

\[ \ddot{w} = f(w, u) \quad \text{and} \quad 0 = g(w, u), \] (13)

with the vector-valued functions $f$ and $g$ and the state vector $\vec{w} = [w, \dot{w}]$. The vectors $\vec{w}$ and $\vec{u}$ contain the Galerkin coefficients whereas $f$ and $g$ result from the boundary conditions (5), (6) or (7) and (9). A linearization of the nonlinear system (13) at the equilibrium is performed and the normalized eigenvalues of the linear system are computed. The eigenvalue with the largest real part is denoted by $\epsilon_s$. If $\epsilon_s$ has a positive real part, the system (12) and (4) with the related boundary conditions is unstable.

Three different types of equilibria are observed depending on the existence of one or two equilibria for non-negative displacement $w$ in the range $0 \leq w \leq L_b/2$. For simplicity, a vanishing offset $w_0 = 0$ is assumed.
One unstable equilibrium $w = 0$ (case 1): The entire area of the permitted cooler range is unstable. This case can occur for moderate tensile loads (boundary condition A) or prestresses (boundary condition B) $N_{xx}$. A slight deviation from $w = 0$ causes $w$ to grow until the strip collides.

One stable equilibrium $w = 0$ (case 2): The entire area of the permitted cooler range belongs to the region of attraction of the equilibrium. A high value $N_{xx}$ leads to this kind of equilibrium.

Two equilibria $w = 0$ and $w \neq 0$ (case 3): The inner equilibrium $w = 0$ is always stable and the outer one $w \neq 0$ is always unstable. The region of attraction of the stable (inner) equilibrium contains the range from $w = 0$ to the outer unstable equilibrium.

Example 1: For the last case, the influence of the strip thickness $h$ and the tensile load $N_{xx}$ on the unstable equilibrium shape is shown in Fig. 9. The offset shift of the strip is set to $w_0 = 0$ and the cooler pipe overpressure is $p = 40 \text{ kN/m}$. Based on (1), the associated cooler fan speed is approximately $n = 1830 \text{ 1/min}$.

For $N_{xx}/b = 30 \text{ kN/m}$, two equilibria are observed (case 3): The inner one $w = 0$ is stable ($e_s = -0.47$) and the outer one $w \neq 0$ is unstable ($e_s = 5.30$). The same applies to $40 \text{ kN/m}$: The equilibrium $w = 0$ is stable ($e_s = -0.41$) and the other one $w \neq 0$ is unstable ($e_s = 6.76$). Both unstable equilibria are shown in Fig. 9. For $30 \text{ kN/m}$ an estimation of the region of attraction is shown as a shaded area. The cooler array is shown as gray shaded box.

For $55 \text{ kN/m}$, only one stable equilibrium $w = 0$ (case 2) with $e_s = -0.35$ exists. The strip cannot become unstable for the values $w$ permitted by the cooler array.

The low tensile load of $15 \text{ kN/m}$ leads to one unstable equilibrium $w = 0$ (case 1) with $e_s = 1.57$. This operating condition must be avoided.

Finally, the same reference displacement $u_L = 6.7 \text{ mm}$ is chosen for different strips. According to (7), this displacement would occur for a $1 \text{ mm}$ thick and $1.65 \text{ m}$ wide strip with a tensile load of $35 \text{ kN}$. The thinnest strip would collide with the cooler array in case of a small disturbance (stability case 1). The remaining two strips will stay stable inside the region of attraction of the stable equilibrium $w = 0$ (case 3). See the remarkable difference between Figs. 10 and 11 which is only caused by the difference of the boundary condition $u_L$.

4.3 Influence of Pressure and Cooler Fan Speed

Example 3: The influence of the cooler pressure on the equilibrium $w \neq 0$ is investigated using the pressure levels $10, 25, 40 \text{ mbar}$. They correspond to the cooler fan speeds $912, 1446, 1830 \text{ 1/min}$, see (1). The simulation results for a thin strip with thickness $h = 0.5 \text{ mm}$ and a tensile load of $20 \text{ kN/m}$ (boundary condition A) are shown in Fig. 12. For $p = 10 \text{ mbar}$, only the equilibrium $w = 0$ exists within the permitted range of the cooler array. The system (13) is linearized about this equilibrium. With $e_s = -1.01$, case (case 3) changes depending on the thickness $h$, the boundary condition A or B, and the load $N_{xx}$. Furthermore, the case of using the same prestress displacement $u_L$ for all strips with different thicknesses is examined.

Example 2: For boundary condition A with a constant tensile load, the strip thickness $h$ has no noticeable influence on the equilibrium. In contrast, however, the tensile load $N_{xx}$ has a significant effect on the equilibrium as can be seen in Fig. 9.

The situation is different for boundary condition B. After prestressing the strip with a total force $N_{xx}$, a certain displacement $u_L$ appears depending on the strip thickness. This unique displacement value is fixed at the upper edge, i.e., $u(L) = u_L$. For an additional strip extension due to a transversal displacement $w$, a thicker strip will exercise a higher resetting force. Therefore, an equilibrium will occur slightly further away from the $x$-axis compared to a thinner strip because the destabilizing effect of the cooler array must also be greater. See the examples shown in Fig. 10 for more details.

![Fig. 10. Unstable equilibria for boundary condition B and various values of $N_{xx}/b$ (solid line: $h = 1.5 \text{ mm}$, dashed line: $h = 1 \text{ mm}$).](image)
4.4 Influence of an Offset Shift

Example 4: An offset shift $w_0$ may be caused by a misalignment between the ideal strip pass line and the cooling sections. The influence on the stable equilibrium position (case 3) for a strip with thickness $h = 1$ mm and a constant tensile load (boundary condition A) of $35$ kN/m is shown in Fig. 13. The cooler pressure is set to $25$ mbar.

Even a minor offset shift is causing a big shift of the stable equilibrium in transversal direction. A positive offset will lead to a drift in positive direction and vice versa. This is a direct consequence of the destabilising effect of the cooler array. The outer equilibria are also affected due to the offset shift. For $w > 0$, a positive offset $w_0$ will move the unstable equilibrium further inwards or, equivalently, it will shrink the region of attraction. The unstable equilibrium for $w = 0$ will be pushed outwards.

Depending on the tensile load $N_{xx}$ and on the pressure level $p$, the entire negative side becomes the region of attraction of the stable equilibrium $w = 0$ in many cases. The unstable equilibria are not shown in this paper.

5. CONCLUSIONS

The most important findings of this study are summarized in the following:

- Depending on different plant parameters, e.g., the tensile load $N_{xx}$ and the pressure level $p$, three different types of equilibria are observed.
- It is necessary that the inner equilibrium is a stable one to ensure a proper strip processing. Otherwise, the strip will collide with the cooler array. The best way to keep the equilibrium stable is to increase the tensile load $N_{xx}$.
- For a constant tensile load (boundary condition A), the strip thickness $h$ has virtually no effect on the equilibrium. This does not apply to the preloaded and fixed strip (boundary condition B).
- Small imperfections, which lead to an offset shift $w_0$ of the strip, can have a huge impact on the stability.

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