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Directional excitation of graphene surface plasmons

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Abstract: We propose a scheme to directionally couple light into graphene plasmons by placing a graphene sheet on a magneto-optical substrate. When a magnetic field is applied parallel to the surface, the graphene plasmon dispersion relation becomes asymmetric in the forward and backward directions. It is possible to achieve unidirectional excitation of graphene plasmons with normally incident illumination by applying a grating to the substrate. The directionality can be actively controlled by electrically gating the graphene, or by varying the magnetic bias. This scheme may have applications in graphene-based opto-electronics and sensing.

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1. Introduction

Since the first exfoliation of graphene ten years ago [1], this two-dimensional material has attracted tremendous research interest, due to its unique electronic [2], mechanical [3], optical [4] and thermal properties [5]. Its high carrier mobility at room temperature makes it a promising material for post-silicon electronics, as well as for photonic and opto-electronic devices. Although an isolated layer of intrinsic graphene interacts rather weakly with light (absorbing only $\sim 2.3\%$ of the incident intensity, independent of frequency [4]), the interaction can be enhanced by external cavity resonances [6–8], or by plasmonic resonances of the graphene surface itself [9–12]. The latter approach, which is the domain of the emerging field of “graphene plasmonics”, produces operating frequencies in the technologically-relevant terahertz to mid-infrared range. Compared to conventional metal surface plasmons, graphene surface plasmons are subject to lower propagation losses [13–15]. They also have the virtue of being highly tunable, via electrostatic or chemical doping of the graphene layer [10, 11].

This paper investigates the interesting possibility of directionally exciting graphene surface plasmons with the aid of a magneto-optical substrate. In order for graphene plasmons to be excited by external illumination, surface modulations are typically needed for wavevector matching. One approach is to pattern the graphene into nano-ribbons, which localizes the plasmon resonances [10–12]. Alternatively, propagating graphene plasmons can be excited by patterning gratings into the substrate [16], or by applying elastic vibrations to the graphene [17, 18]. In principle, very high coupling efficiency (on the order of 50%) can be achieved [17]. These methods excite plasmons in both directions along the grating; for numerous switching applications, it would be useful to be able to control the propagation direction of the plasmons. In the literature on conventional surface plasmons, several methods for directional excitation have recently been explored [19–25]. However, it is challenging to apply most of these methods to graphene plasmons, due to graphene’s two-dimensional nature, as well as the technical difficulty of patterning a meta-surface onto graphene without harming the optical sheet conductivity by edge scattering [12].

The system we investigate consists of a graphene layer on a magneto-optical substrate magnetized parallel to the surface. Unlike other recent papers on magnetic graphene plasmons [26–30], we do not magnetize the graphene sheet perpendicular to the plane, which would induce Landau levels and an off-diagonal current response [31]. As discussed below, such schemes do not lead to the desired phenomenon of directional in-plane excitation of bulk plasmons. In the present system, the propagation of the graphene plasmon is made nonreciprocal by the penetration of the plasmon mode into the magneto-optical substrate, which is magnetically biased parallel to the surface and perpendicular to the direction of propagation. This...
configuration is reminiscent of the work of Yu et al. [32], who showed that a surface plasmon at the interface between a dielectric and a magnetic metal (likewise biased parallel to the surface) exhibits an asymmetric dispersion relation. Remarkably, because that system has a dispersion relation with a frequency cutoff, it acts as a unidirectional plasmonic waveguide over a finite frequency bandwidth below the cutoff. In the case of graphene plasmons, it is a well-known fact that no such cutoff exists [13]. Nonetheless, directionality can be enforced at specific frequencies by the application of a grating. Unlike previous works, where the grating was achieved by patterning the graphene into nano-ribbons [33,34], we consider a contiguous graphene layer lying on a modulated substrate surface. Thus, light incident at an appropriately-chosen frequency can excite graphene plasmons propagating in one direction along the surface. For a fixed operating frequency, it is even possible to actively reverse the direction of excitation, either by switching the magnetic field direction, or (more interestingly) by varying the Fermi level of the graphene layer. Such a device may have applications in graphene-based opto-electronic and photonic devices, such as optical absorbers, nano-sensors, and molecular detectors.

2. Asymmetric dispersion relation

Consider a graphene sheet lying on a magneto-optical substrate, as shown schematically in Fig. 1(a). A grating is etched onto the surface, with period $\Lambda$. If the modulation is sufficiently weak, it will not significantly affect the dispersion relation of surface plasmon modes [35,36]. Thus, we can derive the plasmon dispersion by taking the limit of zero modulation (i.e., a flat surface). When a magnetic field applied in the $\hat{y}$ direction, the relative dielectric constant of the substrate (medium 1) is

$$\varepsilon = \begin{bmatrix} \varepsilon_1 & 0 & i\alpha \\ 0 & \varepsilon_\parallel & 0 \\ -i\alpha & 0 & \varepsilon_1 \end{bmatrix}. \quad (1)$$

Here, $\varepsilon_1$ and $\varepsilon_\parallel$ are the dielectric components perpendicular to and parallel to the magnetization; $\alpha$ is the magneto-optical component. Note that the magnetic field is applied in the $\hat{y}$ direction (parallel to the surface), so it does not split the electronic states into Landau levels, unlike the case where the magnetic field is applied through the graphene sheet [26,27,31].
the graphene, the dielectric constant is $\varepsilon_2$ (medium 2). The graphene layer has isotropic sheet conductivity $\sigma$.

We look for surface plasmon modes where the electric and magnetic fields in medium 1 and 2 have the form

$$\vec{E}_j(x,z) = (E_{jx},0,E_{jz})e^{iqx}e^{-k_j|z|},$$

$$\vec{H}_j(x,z) = (0,H_{jy},0)e^{iqx}e^{-k_j|z|},$$

where $q$ denotes the wavevector in the $\hat{x}$ direction, $k_j$ is the decay constant in the $\hat{z}$ direction, for medium index $j = 1, 2$. We plug these expressions into Maxwell’s equations, assume all the time-dependent fields are harmonic with frequency $\omega$, and impose the boundary conditions $E_{1x} = E_{2x}$ and $B_{1y} = B_{2y} - \sigma E_{1x}$ along the graphene layer. The resulting dispersion relation is:

$$\varepsilon_2 k_2^2 + \varepsilon_1^2 - \alpha^2 k_1 \varepsilon_1 + \frac{i \sigma \omega \varepsilon_0}{\omega} = 0,$$

where $\varepsilon_0$ is the permittivity of free space and

$$\begin{align*}
k_1 &= \sqrt{q^2 - \left(\frac{\varepsilon_1^2 - \alpha^2}{\varepsilon_1}\right) \frac{\omega^2}{c^2}}, \\
k_2 &= \sqrt{q^2 - \varepsilon_2^2 \frac{\omega^2}{c^2}}.
\end{align*}$$

Evidently, $k_1$ and $k_2$ only depend on the absolute value of $q$, and do not depend on the direction of propagation. However, the second term of Eq. (4) has a denominator which involves $q$ rather than $q^2$. This is the source of the magneto-optically induced asymmetry.

The AC sheet conductivity of graphene can be modeled as [36]

$$\sigma(\omega) = \frac{e^2 E_F}{\pi \hbar^2} \frac{i}{\omega + i/\tau},$$

where $E_F$, $\tau$, $\hbar$, and $e$ are the Fermi level, damping time, Planck constant, and electron charge respectively. Figure 1(b) shows the asymmetric dispersion relation computed numerically from Eqs. (4)-(7), assuming frequency-independent dielectric components.

We will work in the “non-retarded” regime, where the mode lies well below the light line and is well-confined [13]. For $1/\tau \ll \omega \ll q c$, Eqs. (4)-(7) simplify to

$$\omega \approx \frac{e^2 E_F}{\pi \hbar^2 \varepsilon_0} \sqrt{\frac{|q|}{\varepsilon_1 + \varepsilon_2 + \alpha}},$$

where $\pm$ denote right and left propagation respectively. For $\alpha = 0$, Eq. (8) reduces to the usual square-root dispersion relation for graphene surface plasmons [13]. For $\alpha \neq 0$, the dispersion relation is asymmetric; for fixed $|q|$, there are two different values for $\omega$. Note that $\alpha$, $\varepsilon_1$, and $\varepsilon_2$ can also depend implicitly on $\omega$.

From Eq. (8), we obtain the frequency difference ratio

$$\frac{\delta \omega}{\omega_0} \sim \frac{\alpha}{\varepsilon_1 + \varepsilon_2},$$

where, for fixed $|q|$, $\delta \omega$ is the frequency difference between right- and left-moving plasmons. This depends only on the strength of the off-diagonal (magneto-optical) components of $\varepsilon$. 

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relative to the diagonal components, in the bulk media. It does not depend on the graphene sheet conductivity, which affects only \( \omega_0 \), the unmagnetized graphene surface plasmon frequency.

For a typical magneto-optical material, the dielectric components defined in Eq. (1) can be modeled by [37–39]

\[
\varepsilon_\parallel(\omega) = \left(1 - \frac{\omega_p^2}{\omega^2 - \omega_c^2}\right) \varepsilon_\infty
\]

\[
\alpha(\omega) = \frac{\omega_p^2 \omega_c}{\omega(\omega^2 - \omega_c^2)} \varepsilon_\infty,
\]

where \( \varepsilon_\infty \) is the limiting permittivity at high frequencies, \( \omega_p \) is the bulk plasma frequency, and \( \omega_c \) is the cyclotron frequency induced by the magnetic bias. Assuming \( \varepsilon_2 = 1 \) and weak magnetization (\( \omega_c \ll \omega, \omega_p \)), combining Eqs. (9)-(11) gives

\[
\delta \omega \sim \omega_H c \cdot \frac{\omega_p^2}{\varepsilon_\infty^2} \frac{\omega_p^2 / \omega_0^2}{1 - \omega_p^2 / \omega_0^2}.
\]

It is useful to compare these results to the “magnetic surface plasmon” which occurs at the interface between a dielectric and a magnetic metal [32]. That situation corresponds to setting \( \sigma = 0 \) in Eq. (4); in order for a confined state to exist in the absence of the conducting layer, the magneto-optical material must then be metallic (\( \varepsilon_1 < 0 \)). In the large-\( q \) regime, the magneto-optical frequency difference is found to be \( \delta \omega \sim \omega_c \), with no leading-order dependence on \( \varepsilon_\infty \) or \( \omega_p \). Because the magnetic surface plasmon’s dispersion relation has a frequency cutoff, propagation becomes unidirectional in a finite frequency range near the cutoff [32]. In the present case, however, the confinement is provided by the graphene layer, and we can take the magneto-optical material to be non-metallic (\( \varepsilon_1 > 0 \)); because the dispersion relation has no cutoff, directionality has to be imposed by other means, such as a grating.

3. Directional coupling

To excite the graphene surface plasmons, we consider applying a weak periodic modulation to the surface of the substrate. The grating couples incident light with transverse wavevector component \( k_0 \) to surface plasmons with wavevector \( k_{spp} = k_0 \pm 2\pi N/\Lambda \), where \( \Lambda \) is the grating period and \( N \in \mathbb{Z}^+ \). In the non-retarded regime, the directionality of the incident light has little effect on the coupling since \( k_0 \ll k_{spp} \), as indicated in Fig. 1(b). Henceforth, we assume normal incidence (\( k_0 = 0 \)) for simplicity.

For nonzero magnetic bias, the incident light couples to left- and right-moving surface plasmons at different resonance frequencies. To demonstrate this effect, we perform full-wave finite element simulations of Maxwell’s equations (using the Comsol Multiphysics software package) for the setup of Fig. 1(a). The results are shown in Fig. 2. For the substrate, we use indium antimonide (InSb), which has been shown to have large magneto-optical response at terahertz and mid-infrared frequencies [37–39]. Its dielectric tensor components can be modeled by Eqs. (10)-(11), with \( \varepsilon_\infty = 15.68 \) and \( \omega_c = eB/m^* \) (where \( m^* = 0.014m_e \) is the effective mass). The bulk plasma frequency is given by \( \omega_p^2 = ne^2/(\varepsilon_\infty m^* \varepsilon_0) \), where \( n = 5.5 \times 10^6 \, \mu \text{m}^{-3} \).

For an operating frequency of 50 THz and magnetic bias of \( B = 1\, \text{T} \), this results in \( \varepsilon_1 \approx 3 \) and \( \alpha \approx 0.5 \). The grating has period \( \Lambda = 250 \, \text{nm} \) and modulation amplitude 40 nm (note that these length scales are sufficiently large that quantum effects can be safely ignored [40]). For numerical purposes, the graphene sheet is modeled as a thin layer of thickness \( d \approx 0.3 \, \text{nm} \) with effective dielectric constant \( \varepsilon_{\text{eff}} = 1 + i\sigma/(\varepsilon_0 \omega d) \).

For the graphene conductivity parameters, we take \( E_F = 1 \, \text{eV} \) and \( \tau = 10^{-12} \, \text{s} \). The Fermi level \( E_F \) is tunable by electrostatic or chemical doping, and our choice of 1 eV is typical [41].
Fig. 2. (a) Absorption spectrum of graphene surface plasmon resonances, obtained by full-wave simulations of the system shown in Fig. 1(a). With zero applied magnetic field (blue triangles), there is a single absorption peak, corresponding to bi-directional excitation of surface plasmons. With a 1T applied magnetic field (red circles), there are two distinct absorption peaks, corresponding to plasmons propagating in the $\pm \hat{x}$ directions. $N$ labels the grating index; the plasmon wavevectors are $\pm 2\pi N/\Lambda$, where $\Lambda$ is the grating period. (b)-(d) Plots of $H_z$ for three resonances; black arrows indicate the local Poynting vector.

As for the damping time $\tau$, at terahertz frequencies it has very weak frequency dependence and is conventionally treated as a constant [36, 42]; our chosen value is typical for graphene on semiconductor substrates, but the value for an actual magneto-optical substrate is not known. In a recent experiment, $\tau$ was found to be substantially reduced in graphene nano-ribbons, due to edge scattering [12], but this does not apply to the present situation since no edges are present.

In Fig. 2(a), we see that in the absence of an applied magnetic field, there are absorption peaks near 37 THz, 53 THz, 65 THz, ..., corresponding to the excitation of surface plasmons for different values of $N$. The field distribution of $H_y$ for the $N = 2$ mode is plotted in Fig. 2(c), showing that it is a tightly-confined surface plasmon mode. The Poynting vectors, indicated by black arrows in this plot, reveal that the mode is symmetric (i.e., zero net energy flow along the $\hat{x}$ axis). When a magnetic field is applied, each absorption peak splits into two, one below the original frequency and one above, with absorption coefficients comparable to the original peak. (The asymmetry between each pair of peaks is likely due to the variation of the coupling efficiency with frequency.) The field distributions for the $N = 2$ modes are plotted in Fig. 2(b) and (d), and the Poynting vectors indicate the modes are directional, transporting energy in the $-\hat{x}$ and $+\hat{x}$ directions respectively. When the direction of the applied magnetic field is reversed, $\alpha$ switches sign. Thus, at a fixed operating frequency, we can actively control the directionality of the excited surface plasmons.

A more interesting way to control the directionality of the excited surface plasmons is to exploit the extraordinary tunability of graphene's electrical properties. The Fermi level $E_F$ can be controlled very precisely by electrical doping (or a combination of electrical and chemical...
Fig. 3. Active control of plasmon directionality. (a) Plasmon resonance peaks, corresponding to left-moving (L) and right-moving (R) plasmons, can be shifted by tuning the graphene Fermi level $E_F$. At a fixed operating frequency (vertical dashes), we excite right-moving plasmons at $E_F = 1$ eV, or right-moving plasmons at $E_F = 1.28$ eV. (b) Power flux through one unit cell, in the $x$ direction (calculated by integrating the Poynting vector) versus $E_F$, for a fixed 56.6 THz illumination frequency. These results were obtained from finite-element simulations, with all other parameters the same as in Fig. 2.

doping). From Eq. (8), increasing $E_F$ shifts all plasmon resonances to higher frequencies. Thus, the propagation direction at a specific frequency can be switched by tuning $E_F$.

An example is shown in Fig. 3. At a chosen operating frequency of 56.6 THz, indicated by vertical dots in Fig. 3(a), there is a right-moving plasmon resonance for $E_F = 1$ eV. As we increase $E_F$, all the plasmon resonances shift rightward, and at $E_F = 1.28$ eV the operating frequency lines up with a left-moving plasmon resonance. Hence, for fixed illumination frequency, the power flux parallel to the surface switches sign with varying $E_F$, as shown in Fig. 3(b). This tunability may be useful for applications in switchable plasmonics.

4. Discussion

The setup we have considered in this paper is different from the one considered in most previous works on magnetic plasmons in graphene, where the magnetic field is applied perpendicular to the plane of the graphene sheet. In that latter setup, the graphene band structure forms Landau levels [26,27,31], resulting in a complicated splitting of the plasmon frequencies [43]. However, this splitting only affects the transmission coefficient of circular polarized incident light; it does not excite the plasmon in a specific in-plane direction, which is the phenomenon we are interested in. Recently, Xiao et al. have studied a setup where the magnetic field is applied in-plane [44]. However, they treated the case of a stack of graphene sheets several microns thick, and considered the magneto-optical effect occurring in that stack, in a manner directly analogous to the magnetic surface plasmons of Ref. [32]. Such a scheme is not practically realizable or relevant to the case of monolayer graphene. In our work, the magneto-optical
effect is due to the substrate material, not the graphene layer.

In our simulations, we have chosen to focus on the simplest mechanism for coupling incident light to the surface plasmons, i.e. by modulating the surface of the magneto-optical substrate. The feasibility of depositing graphene onto such a surface is an open experimental question; furthermore, it is not known whether the conductive properties of graphene will be drastically altered by the choice of substrate [45–47]. We emphasize, however, that details about the implementation of the grating mainly affect the coupling efficiency, and largely do not alter the analysis of the dispersion relation of magneto-optical graphene surface plasmons; for instance, one might instead deposit a dielectric grating on top of the graphene.

In conclusion, we have presented a simple scheme for directionally exciting graphene surface plasmons, based on the asymmetry in the surface plasmon dispersion relation due to a magneto-optical substrate. The directionality can be actively controlled, such as by electrically gating the graphene layer. This phenomenon might be useful for more complex graphene plasmonic devices, such as using the graphene plasmon to enhance the transverse magneto-optical Kerr effect [48, 49]. It would also be interesting to explore the possibility of using an alternative conducting material, such as a metallic thin film, in place of the graphene; the surface plasmons which arise in such dielectric/thin metal/magneto-optical dielectric structures may have useful applications outside the context of graphene-based technologies.

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