Spin Wave Based 4-2 Compressor

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By their very nature, Spin Waves (SWs) consume ultra-low amounts of energy, which makes them suitable for ultra-low energy consumption applications. In addition, a compressor can be utilized to further reduce the energy consumption and enhance the speed of a multiplier. Therefore, we propose a novel energy efficient SW based 4-2 compressor consisting of 4 XOR gates and 2 Majority gates. The proposed compressor is validated by means of micromagnetic simulations and compared with the state-of-the-art SW, 22 nm CMOS, Magnetic Tunnel Junction (MTJ), Domain Wall Motion (DWM), and Spin-CMOS technologies. The performance evaluation shows that the proposed compressor consumes 2.5x less and 1.25× less energy than the 22 nm CMOS and the conventional SW compressor, respectively, whereas it consumes at least 3 orders of magnitude less energy than the MTJ, DWM, and Spin-CMOS designs. Furthermore, the compressor achieves the smallest chip real-estate. In summary, the performance evaluation of our proposed compressor shows that the SW technology has the potential to progress the state-of-the-art circuit design in terms of energy consumption and scalability.

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I. INTRODUCTION

Complementary Metal Oxide Semiconductor (CMOS) downscaling has been efficient to meet the exploding market requirements for highly efficient computing platforms that process the raw data resulting from the information technology revolution\(^1\). However, CMOS downscaling becomes very difficult as we approach the end of Moore’s law because of the leakage, cost, and reliability walls\(^2\). Therefore, researchers have explored different technologies including spintronics\(^3\). One of the spintronic promising technologies is the Spin Wave (SW) technology because it has ultra-low energy consumption, acceptable delay, and high scalability\(^4\)–\(^8\). As a result, there is a strong interest in designing SW based circuits.

Researchers have designed different logic gates and circuits using SWs\(^5\)–\(^7\),\(^9\)–\(^14\). A Mach-Zehnder interferometer was utilized to build the first experimental SW NOT gate\(^9\). Afterwards, single output Majority, (N)AND, (N)OR, and X(N)OR gates were built using Mach-Zehnder interferometers\(^9\), whereas multi-output logic gates were suggested\(^7\),\(^10\),\(^12\). Moreover, multi-frequency logic gates were reported\(^6\),\(^11\). On a bigger scale, multiple circuits have been introduced at the conceptual\(^13\), simulational\(^5\), and also practical millimeter scale level\(^14\). To conclude, SW circuit design is still in its genesis stage. Therefore, the design, validation and demonstration of SW based circuits at different complexity scales is of great interest to progress SW computing.

Driven by the aforementioned information, we propose, validate, and assess a novel SW based 4-2 compressor consisting of 4 XOR and 2 Majority gates. In the following, we summarize the main contributions of the paper:

- Designing a novel SW 4-2 compressor.
- Validating the proposed 4-2 Compressors by means of micromagnetic simulations.
- Demonstrating the compressor superiority by comparing its performance with the state-of-the-art SW, 22nm CMOS, Magnetic Tunnel Junction (MTJ), Domain Wall Motion (DWM), and Spin-CMOS technologies. The evaluation results show that the proposed compressor consumes 1.25x less energy than the conventional SW compressor, and 2.5x less energy than the 22nm CMOS counterparts. In addition, it outperforms the MTJ, DWM, and Spin-CMOS designs by at least 3 orders of magnitude. Furthermore, it achieves the smallest chip real-estate.
The paper is organized as follows. We explain the SW background and computing paradigm in Section II. Next, we illustrate the proposed compressor in Section III, and present the simulation setup, results, and performance evaluation in Section IV. Section V concludes the paper.

II. SPIN WAVE BASED TECHNOLOGY FUNDAMENTAL AND COMPUTING PARADIGM

The magnetization dynamics in a ferro- or ferrimagnetic material is described by the Landau-Lifshitz-Gilbert (LLG) equation:

\[
\frac{d\vec{M}}{dt} = -|\gamma| \mu_0 \left( \vec{M} \times \vec{H}_{\text{eff}} \right) + \alpha \frac{M_s}{M} \left( \vec{M} \times \frac{d\vec{M}}{dt} \right),
\]

where \(\gamma\) is the gyromagnetic ratio, \(\mu_0\) the vacuum permeability, \(M\) the magnetization, \(M_s\) the saturation magnetization, \(\alpha\) the damping factor, and \(H_{\text{eff}}\) the effective field consisting of the external field, the exchange field, the demagnetizing field, and the magneto-crystalline field.

For small magnetic disturbances, the LLG equation predicts wave-like magnetic motion. These wave-like solutions are called Spin Waves (SWs), reflecting collective excitations of the magnetization within the magnetic material.

The SW amplitude and phase can be used to encode information at different frequencies. Moreover, the processing of this information is performed by the interference principle. For example, if two SWs with the same amplitude, wavelength, and frequency meet in the waveguide, they interfere constructively if they have the same phase, \(i.e.\) \(\Delta \phi = 0\), and destructively if they have opposite phases, \(i.e.\) \(\Delta \phi = \pi\). In addition, SWs naturally support Majority gates because the interference of an odd number of SWs is based on the Majority decision. For instance, if 3 SWs with the same amplitude, wavelength, and frequency meet in the same waveguide, the interference result is a SW with phase 0 if at least 2 SWs have a phase of 0, whereas the interference result is a SW with phase \(\pi\) if at least 2 SWs have a phase of \(\pi\). Note that such an implementation in CMOS technology requires 18 transistors whereas it can be directly implemented in SW technology. In this paper, logic 0 corresponds to a SW with phase 0, whereas logic 1 corresponds to a SW with phase \(\pi\).

SW device consists of four main stages: i) excitation stage, ii) waveguide, iii) functional stage, and iv) detection stage. At the excitation stage, SW is excited by means of voltage driven cells such as Magneto-Electric (ME) cells or current driven cells such as inductive
antennas. After SW excitation, SW propagates through the waveguide which can be made of different material such as Permalloy, and CoFeB. At the functional stage, the SW can be manipulated, normalized, amplified, or interfered with other SWs. Finally, the resultant SW is captured at the detection stage, which can be similar or different than the ones utilized at the excitation stage. Two different techniques can be utilized to capture the SW: phase detection and threshold detection. In the phase detection, the resultant SW phase is compared with a predefined phase, if its phase is 0, the output is logic 0, and otherwise, logic 1. On the other hand, in the threshold detection, the dynamic magnetization amplitude is compared with a predefined threshold, i.e., if the amplitude is larger than the predefined threshold, the output is logic 0, and otherwise, logic 1.

III. SW 4-2 COMPRESSOR

The fast multiplier consists of three main stages: partial product generator, partial products reducer, and final production computer; the main part of the energy consumption and delay originates from the partial product stage. This can be optimized by utilizing a 4-2 compressor in the partial products reducer stage of the fast multiplier. Therefore, we built a SW 4-2 compressor.

Figure 2 presents the proposed 4-2 compressor consisting of 5 inputs $X_1, X_2, X_3, X_4$, and $C_i$ and 3 outputs $C_{o1} = \text{MAJ}(X_1, X_2, X_3)$, $C_{o2} = \text{MAJ}(\text{XOR}(\text{XOR}(X_1, X_2), X_3), X_4, C_i)$, and $S = \text{XOR}(\text{XOR}(\text{XOR}(\text{XOR}(X_1, X_2), X_3), X_4), C_i)$ in addition to 3 intermediate cells $I_1, I_2$, and $I_3$, which are repeaters to receive and excite the SWs with the suitable amplitude.
and phase.

In order to ensure the correct functionality of the proposed 4-2 compressor, all SWs must be excited at the same amplitude, wavelength, and frequency. The SW wavelength must be larger than the waveguide width to simplify the interference pattern. Moreover, the structure must be designed carefully to guarantee the correct functionality of the compressor because the structure’s dimension affects the interference results. For example, if constructive interference is required at the intersection point when the waves have the same phase and destructive interference otherwise, then the device dimensions $d_1, d_2, d_3, d_5, d_6, d_7,$ and $d_8$ must equal to $n\lambda$ where $n = 0, 1, 2, \ldots$ Note that this is the case in our design. The outputs $C_{o1}$ and $C_{o2}$ must be located at a specific position as they are based on phase detection. Hence, by changing its location, it is feasible to extract the inverted output or the non-inverted output. For example, if the desired result is to capture the non-inverted output, the distance $d_4$ must equal $n\lambda$ which is the case for $C_{o1}$ and $C_{o2}$. On the other hand, as the output $S$ is detected based on threshold detection, the resultant SW is compared with a predefined threshold value as previously discussed. To detect the largest possible SW amplitude, the output $S$ must be located as close as possible to the interference point, i.e., $d_9$ must be as small as possible.

The proposed 4-2 SW compressor works as follows:

- **Carry-out1 output $C_{o1}$**: The SWs excited at $X2$ and $X3$ interfere constructively or destructively depending on their phase at the intersection point. Then the SW interference result propagates further through the waveguide and interferes with the SW
excited at X1 at the intersection point between the waveguides. Finally, the resultant SW is captured at \( C_{o1} \) based on phase detection.

- **Carry-out2 output \( C_{o2} \):** The SWs excited at X2 and X3 interfere constructively or destructively depending on their phase at the intersection point. After that, the resultant wave is received by repeater I1 which will excite a SW with a suitable phase depending on the received SW magnetization. If the received SW magnetization is larger than a threshold, a SW with phase of 0 will be excited, and a SW with phase of \( \pi \) will be excited, otherwise. Then, the SW excited from I1 interferes with the SW excited from X3. Next, the resultant SW will be received by the repeater I2 which will excite a SW with a suitable phase depending on the received SW magnetization at the intersection point between the waveguides. Meanwhile, the SWs excited from X4 and Ci will interfere at the intersection point. Finally, the resultant SW will interfere with the SW excited from I2, and the result will be captured by \( C_{o2} \) based on phase detection.

- **Sum output S:** The SWs excited from X4 and Ci will interfere at the intersection point between the two waveguides, and the result will be detected by repeater I3. Next, repeater I3 will excite a SW with a suitable phase depending on the received SW magnetization as previously discussed. Finally, the output S will capture the results of the interference between SWs excited from I2 and I3 based on threshold detection.

**IV. SIMULATION SETUP, RESULTS AND PERFORMANCE EVALUATION**

**A. Simulation Setup**

We utilized the following parameters to validate the proposed structure by MuMax3\textsuperscript{16}: 50 nm wide and 1 nm thick Fe\textsubscript{60}Co\textsubscript{20}B\textsubscript{20} waveguide with saturation magnetization \( M_s \) of 1.1 MA/m, damping constant \( \alpha \) of 0.004, and exchange stiffness \( A_{exch} \) of 18.5 pJ/m\textsuperscript{17}. We excited the SWs with a 10 GHz Gaussian pulse with sigma of 500 ps to save energy, guarantee a single frequency SW excitation, and achieve high group velocity. The wavenumber \( k \) is determined from the SW dispersion relation, which makes the wavelength equals
Figure 3 presents the proposed compressor carry-out1 $C_{o1}$ MuMax3 simulation results for \( \{X_1,X_2,X_3\} = \{0,0,0\}, \{0,0,1\}, \{0,1,0\}, \{0,1,1\}, \{1,0,0\}, \{1,0,1\}, \{1,1,0\}, \text{ and } \{1,1,1\} \), respectively. Inspecting the figure, the $C_{o1}$ is captured correctly based on phase detection. For example, $C_{o1} = 0$ for \( \{I_1,I_2,I_3\} = \{0,0,0\}, \{0,0,1\}, \{0,1,0\}, \text{ and } \{1,0,0\} \), whereas $C_{o1} = 1$ for \( \{X_1,X_2,X_3\} = \{0,1,1\}, \{1,0,1\}, \{1,1,0\}, \text{ and } \{1,1,1\} \) at time=$2.25 \text{ ns}$.

Table I presents the normalized magnetization of the SW received by the repeater $I_1$ and the SW excited by $I_1$ for different input combinations \( \{X_2,X_3\} = \{0,0\}, \{0,1\}, \{1,0\}, \text{ and } \{1,1\} \), respectively. Note that the threshold technique is used to detect and excite the SW at $I_1$ such that if the SW magnetization is larger than the threshold, $I_1$ excites a SW with $\phi = 0$, whereas otherwise, $I_1$ excites a SW with $\phi = \pi$. The threshold is calculated by averaging the two nearest cases, i.e. \( \{X_2,X_3\} = \{1,0\}, \{1,1\} \), resulting in $0.585$ for this case.
TABLE I. Normalized SW Magnetization at I1

| Inputs (X2X3) | Normalized SW Magnetization received by I1 | SW excited by I1 |
|---------------|------------------------------------------|-----------------|
| 00            | 1                                        | SW with $\phi = 0$ |
| 01            | 0.18                                     | SW with $\phi = \pi$ |
| 10            | 0.18                                     | SW with $\phi = \pi$ |
| 11            | 0.99                                     | SW with $\phi = 0$ |

TABLE II. Normalized SW Magnetization at I2

| Inputs (X1I1) | Normalized SW Magnetization received by I2 | SW excited by I2 |
|---------------|------------------------------------------|-----------------|
| 00            | 1                                        | SW with $\phi = 0$ |
| 01            | 0.65                                     | SW with $\phi = \pi$ |
| 10            | 0.64                                     | SW with $\phi = \pi$ |
| 11            | 0.99                                     | SW with $\phi = 0$ |

Inspecting the table, we can see that the SW magnetization received by $I_1$ is larger than 0.585 for the input combinations $\{X_2, X_3\} = \{0,0\}$, and $\{1,1\}$, whereas the SW magnetization received by $I_1$ is less than 0.585 for the input combinations $\{X_2, X_3\} = \{0,1\}$, and $\{1,0\}$.

The same reasoning holds for $I_2$ for which the results are presented in Table II. Here, the threshold is set to 0.82 which is the average of the two cases $\{X_2, X_3\} = \{0,1\}$, and $\{1,1\}$. Inspecting the table, we can see that the SW magnetization received by $I_2$ is larger than 0.82 for the input combinations $\{X_1, I_1\} = \{0,0\}$, and $\{1,1\}$, whereas the SW magnetization received by $I_2$ is less than 0.82 for the input combinations $\{X_1, I_1\} = \{0,1\}$, and $\{1,0\}$. After that, the same results are obtained for $C_{o2}$ which is detected based on phase detection as $C_{o1}$, and $I_3$ and $S$ which are detected based on threshold detection as $I_1$ and $I_2$ with the same analysis.

Therefore, the micromagnetic simulation results demonstrated that the 4-2 SW compressor is functioning correctly.
Performance Evaluation

In order to assess the performance of the proposed 4-2 SW compressor and see the potential of such an approach, we evaluate it and compare it with the state-of-the-art SW, 22 nm CMOS\textsuperscript{18}, Magnetic Tunnel Junction (MTJ)\textsuperscript{19}, Domain Wall Motion (DWM)\textsuperscript{19}, and Spin-CMOS\textsuperscript{19} technologies in terms of energy, delay, and area. We have made the following assumptions for the performance evaluation\textsuperscript{5}: (i) The excitation, detection, and repeater cells are Magnetoelectric (ME) cells, and their power consumption, and delay are 34 nW, and 0.42 ns, respectively. (ii) SWs do not consume noticeable energy while interfering with each other or propagating in the waveguide. Note that these assumptions might need re-evaluation in the near future as SW technology is still in its infancy stage.

Table III presents the performance evaluation of the proposed compressor, and the comparison with the state-of-the-art. As it can be observed from the table, the proposed SW compressor consumes 2.5x less energy than the 22 nm CMOS counterpart while requiring 119x more delay\textsuperscript{18}. In addition, the proposed SW compressor consumes at least 3 orders of magnitude less energy than the MTJ, DWM, and Spin-CMOS counterparts, while requiring 1.84x, and 1.26 more delay, and 1.28x less delay than the MTJ, DWM, and Spin-CMOS counterparts, respectively\textsuperscript{19}. When compared with the conventional SW 4-2 compressor, which is two cascaded full adders, the proposed SW 4-2 compressor consumes 1.25x less energy than the conventional SW 4-2 compressor while needing 1.22x less delay. Moreover, the proposed compressor requires the least number of devices in comparison with the other designs as can be seen in Table III. Note that the SW delay can be improved by using other materials which have higher group velocity.

We assessed the proposed SW compressor on an application level utilizing the JPEG compression algorithm to see the potential of such an approach in larger scale. In the JPEG algorithm\textsuperscript{20}, DCT and IDCT can be implemented using the 4-2 compressor\textsuperscript{19}. If we implemented the DCT and IDCT by means of the proposed 4-2 SW compressor, we expect to achieve ultra-low-energy consumption. As we discussed previously, the proposed compressor consumes 3 magnitude orders less energy than the Spin-CMOS counterpart which indicates that the DCT/IDCT based on the proposed 4-2 SW compressor will consume at least 3 orders of magnitude less energy than the DCT/IDCT based on the Spin-CMOS 4-2 SW compressor\textsuperscript{19}.
TABLE III. 4-2 Compressor Performance Comparison

| Design  | Technology | Energy (fJ) | Delay (ns) | Device No. |
|---------|------------|-------------|------------|------------|
| 18      | CMOS       | 0.4         | 0.048      | 38         |
| 19      | MTJ        | 85680       | 20.4       | 76         |
| 19      | DWM        | 630         | 3.7        | 58         |
| 19      | Spin-CMOS  | 667         | 6          | 68         |
| Conventional SW | Spin Wave | 0.2     | 5.72       | 14         |
| Proposed SW  | Spin Wave | 0.16      | 4.68       | 11         |

In this paper, our main goal is to propose and validate the SW compressor as a proof of concept without considering thermal noise and variability effects. However, in\textsuperscript{21}, it was presented that the thermal noise, the edge roughness and the waveguide trapezoidal cross section do not have noticeable effects on the gate’s functionality. Therefore, we expect that the thermal noise and variability will have limited effect on the compressor. Nevertheless, we will investigate such phenomena in the future.

It was shown that SW technology can be very effective and has the requirements to progress the state-of-the-art in terms of energy consumption and scalability. However, some open issues are still to be solved\textsuperscript{4}. For example, although Magneto-Electric (ME) cells seem to be the right choice for the SW excitation and detection, their efficient behavior is not yet been experimentally realized. Moreover, although SW technology is highly scalable as the only limitation for a SW device scalability is the SW wavelength, the SW has not yet been distinguished from the noise at the nano-scale\textsuperscript{4}. However, we are sure that the industry, as always, will find its way to efficient nanoscale SW devices and benefit from the SW computing paradigm.

V. CONCLUSIONS

We proposed and validated by means of micro-magnetic simulation a novel 4-2 Spin Wave (SW) compressor. The proposed compressor was assessed and compared with the state-of-the-art SW, 22 nm CMOS, Magnetic Tunnel Junction (MTJ), Domain Wall Motion (DWM), and Spin-CMOS technologies. The evaluation result showed that the proposed compressor consumed 2.5x less energy than 22 nm CMOS counterpart. In addition, it outperformed
the MTJ, DWM, and Spin-CMOS designs by at least 3 orders of magnitude. Moreover, it consumed 1.25x less energy than the conventional SW compressor. Furthermore, it achieved the smallest chip real-estate. To conclude, the performance evaluation shows that SW technology has the potential to further progress the circuit design in terms of energy and scalability.

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REFERENCES

1. N. D. Shah et al., JAMA (2018).
2. N. Z. Haron et al., in Design and Test Workshop, IDT (IEEE, 2008) pp. 98–103.
3. S. Agarwal et al., “International roadmap of devices and systems 2017 edition: Beyond cmos chapter.” Tech. Rep. (Sandia National Lab.(SNL-NM), United States, 2018).
4. A. Mahmoud, F. Ciubotaru, F. Vanderveken, A. V. Chumak, S. Hamdioui, C. Adelmann, and S. Cotofana, Journal of Applied Physics 128, 161101 (2020), https://doi.org/10.1063/5.0019328.
5. A. Mahmoud, F. Vanderveken, C. Adelmann, F. Ciubotaru, S. Cotofana, and S. Hamdioui, IEEE Transactions on Circuits and Systems I: Regular Papers 68, 536 (2021).
6. A. Mahmoud, F. Vanderveken, F. Ciubotaru, C. Adelmann, S. Cotofana, and S. Hamdioui, in 2020 Design, Automation Test in Europe Conference Exhibition (DATE) (2020) pp. 642–645.
7. A. Mahmoud, F. Vanderveken, C. Adelmann, F. Ciubotaru, S. Cotofana, and S. Hamdioui, 2020 IEEE Computer Society Annual Symposium on VLSI (ISVLSI) , 60 (2020).
8. A. Mahmoud, F. Vanderveken, C. Adelmann, F. Ciubotaru, S. Hamdioui, and S. Cotofana, in 2021 22nd International Symposium on Quality Electronic Design (ISQED) (2021) pp. 54–59.
9. M. P. Kostylev et al., Appl. Phys. Lett. 87, 153501 (2005).
10. A. Mahmoud, F. Vanderveken, C. Adelmann, F. Ciubotaru, S. Hamdioui, and S. Cotofana, AIP Advances 10, 035119 (2020).
11. A. N. Mahmoud, F. Vanderveken, C. Adelmann, F. Ciubotaru, S. Hamdioui, and S. Cotofana, IEEE Transactions on Magnetics 57, 1 (2021).
12. A. Mahmoud, F. Vanderveken, C. Adelmann, F. Ciubotaru, S. Hamdioui, and S. Cotofana, in 2020 IEEE 38th International Conference on Computer Design (ICCD) (2020) pp. 332–335.
13. A. Khitun et al., Journal of Applied Physics 110, 034306 (2011).
14. F. Gertz et al., IEEE Trans. Magn. 51, 1 (2015).
15. J. Mori et al., IEEE Journal of Solid-State Circuits 26, 600 (1991).
16. A. Vansteenkiste et al., AIP Advances 4, 107133 (2014).
17. T. Devolder et al., Phys. Rev. B 93, 024420 (2016).
18. A. Arasteh, M. Hossein Moaiyeri, M. Taheri, K. Navi, and N. Bagherzadeh, Integration 60, 224 (2018).
19. S. Angizi, H. Jiang, R. F. DeMara, J. Han, and D. Fan, IEEE Transactions on Nanotechnology 17, 795 (2018).
20. G. K. Wallace, IEEE Trans. on Consumer Electronics 38, xviii (1992).
21. Q. Wang, P. Pirro, R. Verba, A. Slavin, B. Hillebrands, and A. Chumak, Science Advances 4 (2018).