An Efficient Reliability-Based Approach for Evaluating Safe Scaled Distance of Steel Columns under Dynamic Blast Loads

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Abstract: Damage to building load-bearing members (especially columns) under explosions and impact are critical issues for structures, given that they may cause a progressive collapse and remarkably increase the number of potential victims. One of the best ways to deal with this issue is to provide values of safe protective distance (SPD) for the structural members to verify, so that the amount of damage (probability of exceedance low damage) cannot exceed a specified target. Such an approach takes the form of the so-called safe scaled distance (SSD), which can be calculated for general structural members but requires dedicated and expensive studies. This paper presents an improved calculation method, based on structural reliability analysis, to evaluate the minimum SSD for steel columns under dynamic blast loads. An explicit finite element (FE) approach is used with the Monte Carlo simulation (MCS) method to obtain the SSD, as a result of damage probability. The uncertainties associated with blast and material properties are considered using statistical distributions. A parametric study is thus carried out to obtain curves of probability of low damage for a range of H-shaped steel columns with different size and boundaries. Finally, SSD values are detected and used as an extensive databank to propose a practical empirical formulation for evaluating the SSD of blast loaded steel columns with good level of accuracy and high calculation efficiency.

Keywords: safe protective distance; safe scaled distance; steel beam-column; dynamic blast load; reliability analysis; Monte Carlo simulation

1. Introduction

Crowded buildings such as schools, shopping venues, stadiums, transportation infrastructure and public locations are well-known attractive targets for terrorist attacks. The disruption of such places has irreversible consequences, including severe casualties and fatalities and negative impact on society [1]. There is a need to identify areas that may be potentially at risk and to take preventive measures to improve their safety and security. In this regard, securing the perimeter of structures or buildings using landscaping or barrier methods is one of the valid risk reduction options recommended in the literature for protecting buildings against terrorist attacks, including vehicle-borne improvised explosive devices [2]. These secure barriers must be installed at the minimum required stand-off distance from a structure, in order to minimize the damage probability of primary structural elements and consequently the risk of progressive collapse. In order to design a blast-resistant building, the design engineer first has to determine blast loads on the building and its structural components. To determine the characteristics and intensity of blast loading, the parameters for explosive charge weight (W) and stand-off distance (R) must be necessarily known. There are several formulas and graphs that can be used to determine blast load parameters, as a function of the scaled distance parameter (Z). The Z parameter, also known as R/W^{1/3} [3], indicates that two charges with similar geometry, ambient...
conditions, explosive composition, but different size (weight) will produce self-similar blast waves as far as their distances $R = Z \times W^{1/3}$ are identical. A much more complete discussion on features and applicability of the scaling law is given in [4]. In [3], the scaled distance parameter is used to assess the safety and resistance of structures under air blast loads. As an example, for un-strengthened buildings, an SSD of 4.46 m/kg$^{1/3}$ is specified from suffering a damage of “approaching to destruction” [5,6]. The SSD parameter, in this context, represents a guide to determine the explosive weight that can be used at a given distance, without exceeding the safe limit states of the structure (allowable support rotation values or damage index, for low damage). It should be noted that the SSD parameter is derived so that probability of failure is lower than an acceptance criterion. The probability of failure, as explained later in Section 3, is a function of capacity and demand called state function. In some cases, the state function can be expressed mathematically, but in most cases it does not have an explicit mathematical closed-form and must be defined by other methods such as FE analysis. When the state function is defined in mathematical form, it is possible to calculate the SSD parameter directly, otherwise an iteration-based method should be used to meet the acceptance criterion (Section 4). The SSD values presented in standards and regulations are usually obtained from blast tests on simple structural models and the effects of structural configuration or material properties are usually disregarded. As such, guidelines can be used for a quick safety assessment of structures, but do not provide clear damage scenarios [6]. Some studies have been performed to also investigate the SPD and SSD of structural elements under blast loads.

The blast performance assessment of structural systems is one of the critical issues for research. Accordingly, the need of empirical but accurate tools in support of design optimization is an ongoing challenge. Among others, Byfield and Paramasivam [7] developed an iterative method to establish the minimum SSD of Reinforced Concrete (RC) columns for a given charge weight, column geometry and material. The iterative process must be repeated until the strength of the column is equal to the dynamic force in it. Thomas et al. [8] implemented MCS method for the reliability analysis of circular RC columns subjected to sequential vehicular impact and blast. Given that the stand-off distance has marked effects on reliability predictions, minimum SPD values have been proposed for selected configurations. Hadianfard and Malekpour [9] evaluated safe explosion distances of a steel column with IPBv220 and length of 3.6 m under different blast scenarios by utilizing the Single Degree of Freedom (SDOF) and FE methods via MCS method. Zhai et al. [10] investigated the blast effects on reticulated domes, proposing a method to determine the SSD based on the intersections of W-R charts and Pressure–Impulse (P–I) curves. Wu and Hao [6,11] numerically derived the SSD for masonry infilled RC frame structures. The presented SSD values for different damage levels (RC frame collapse, side wall collapse, front wall collapse and excessive damage) were compared with the corresponding estimates by the US DoD [5] and ASCE [12] technical documents. A simple approximate method was proposed by Dorofeev for unconfined hydrogen explosions in three hypothetical obstructed areas with different congestion levels. Based on [13], a number of different safety distance relationships were stipulated depending upon the receptor under consideration, comprising storage distances, process building distances and public building and traffic distances.

To provide a robust background and comprehensive feedback for civil engineering applications, experimental and theoretical investigations on the effects of blast loads on steel structural members have been also reported in [14–17]. Bao and Li [18] focused on the residual axial capacity of square RC columns, while the study in [19] was dedicated to H-section steel columns. A number of numerical investigations used equivalent SDOF systems and FE for primary members [16,20–32]. Besides, the uncertainty of input variables for blast load parameters and material properties (but also geometrical parameters and FE modelling errors [33]) can severely affect the predicted structural response. As such, probabilistic methods are preferred to support a more holistic risk-based approach [34–37]. Several studies have been focused on the reliability analysis of selected structures, such as RC buildings [38,39], steel structures [40], RC slabs [36,41], RC columns [35,42–44], RC
Building structures are complex systems involving various types of materials and components. Common building elements include wall panels [33,45], RC beams [46], composite walls [47], masonry walls [48], profiled wall structures [49], clamped aluminum plate [50] and steel columns [51,52], by considering the uncertainties of input variables related to material properties and blast load parameters. Stewart et al. explored the reliability analysis of structures under blast [33,35,43,44] and supported the definition of a general framework for quantitative probabilistic risk assessment of structures subjected to blast [53–56]. Most of those studies have been developed based on MCS method along with SDOF, Multi Degree of Freedom (MDOF) and full 3D FE models. In [52], a methodology based on structural reliability analysis using MCS and explicit FE modelling (shell element formulation) was proposed for determining the damage probability of H-shape steel columns (IPBv 200 section) under various blast scenarios. It was shown that the time required in a probabilistic analysis for iterations of 1000 and 300 can be expected to be about 100 and 30 h. Such a run time may be acceptable for a single reliability analysis, but it is not suitable for SSD calculations that require a trial-and-error process with several reliability analyses. In this regard, a parametric analysis was performed in [57] to capture the effect of several FE modelling techniques (based on solid, shell or beam elements), blast intensity (medium and high levels) and supports (pinned or fixed ends), on damage evaluation assessment. It was proved that the beam formulations can offer good results for the calculation of the residual axial capacity of blast loaded steel columns, with high computational efficiency.

As mentioned above, recommending the minimum SSD is of high practical interest, especially for the design of structures in congested urban areas. Once SSD is known, the corresponding SPD can be easily calculated as a function of SSD and W. Although the blast dynamic behavior of structures has been largely investigated, the SSD of axially preloaded columns has been rarely considered and, to date, no comprehensive studies have been conducted. In this regard, this paper represents an effort toward the definition of a reliable and efficient methodology based on reliability analysis along with explicit FE approach (using beam element formulation) to determine the SPD and SSD for blast loaded steel columns. The proposed strategy, as shown, can be extended to different structural members (or assemblies) under the effect of a given explosion. In more detail, reliability analyses are carried out to obtain the curves of probability of low damage for a set of H-shape steel columns with different cross sections (IPB180 to IPB500), lengths (2.8, 3.2, 3.6 and 4.0 m) and boundary conditions (pinned or fixed ends), under different explosive charge weights. Afterward, using the obtained curves of probability of low damage, the SSD are extracted for the selected configurations, to present a correlation between SSD and several input parameters (such as the explosive charge weight and the initial axial capacity of a given column) and derive some useful empirical formulas for practical design. An illustrative calculation example is finally discussed, in order to highlight the applicability of the proposed equations for calculating SSD and SPD of steel columns under blast loads.

2. FE Numerical Analysis and Failure Assessment

2.1. Steel Columns

A set of explicit FE models is developed using LS-DYNA software [58], to examine the blast loaded behavior of steel columns with different boundary conditions. As a reference, the limit pinned and fixed ends are considered. To characterize steel, MAT_PLASTIC_KINEMATIC material model is used. This constitutive model can adequately describe the isotropic and kinematic hardening plasticity, with the inclusion of strain rate effects based on the Cooper–Simonds relationship, that is [59–61]:

$$DIF = 1 + \left( \frac{\dot{\varepsilon}}{C} \right)^{\frac{1}{P}}$$

where $\dot{\varepsilon}$ is the material strain rate, DIF is the dynamic increase factor and C and P are constant coefficients that were set to 40.4 and 5 for mild steel [61,62]. The stress–strain curve provided by MAT_PLASTIC_KINEMATIC material model is shown in Figure 1,
where \( L_0 \) and \( L_1 \) are undeformed and deformed lengths of uniaxial tension specimen, respectively. Furthermore, \( E_s, F_y, E_t, \sigma_l \) and \( \epsilon_l \) are the modulus of elasticity, yield stress, the slope of the bilinear stress strain curve in strain hardening region, true stress and true strain, respectively. Furthermore, kinematic, isotropic, or a combination of kinematic and isotropic hardening may be specified by varying \( \beta' \) between 0 and 1 as shown in Figure 1 [58].

![Stress–strain curve of MAT_PLASTIC_KINEMATIC model used for steel material](image)

**Figure 1.** Stress–strain curve of MAT_PLASTIC_KINEMATIC model used for steel material [58].

It should be noted that strain hardening was not considered in this study and the value of \( E_t \) was set to zero (\( E_t = 0 \)). Such a choice was derived from earlier preliminary sensitivity studies where the results showed that strain hardening has no significant effect on residual axial capacity of a steel column [63]. For sake of conciseness, the aforementioned results are not included in the discussion herein reported.

The Hughes–Liu beam element formulation is used for the FE modelling of the selected steel columns [57,64]. There is an integration refinement factor in Hughes–Liu beam element formulation to determine integration points throughout a cross section. The number of integration points can vary depending on the desired accuracy required. A greater number of integration points can also more accurately represent the structural response. In this study \( k \) was set to 5 (\( k = 5 \)) following carried out sensitivity analyses that are not presented in the discussion herein for sake of brevity. A schematic drawing of the typical FE modelling of steel columns (as columns of a building (not columns of a boundary wall)) with H-shape cross section and \( k = 2 \) is shown in Figure 2.

![Integration point numbering](image)

**Figure 2.** FE numerical modelling of H-section steel column with Hughes–Liu beam elements: (a) cross section geometry; (b) integration point numbering; (c) section example for \( k = 2 \).
Although the use of beam elements is notoriously deficient for simulating the effects of local buckling phenomena or shear damage mechanisms induced by blast loads, this choice can significantly improve the calculation efficiency of simulations (compared to shell and solid elements) when the global behavior prediction prevails on local behaviors. This advantage is further appreciated when the time reduction is a relevant issue, like in the case of reliability analysis.

2.2. Nature of Blast Loading

The magnitude of blast waves due to terrorist attacks can be generally classified in the number of explosive packs (portable by humans) and different types of used vehicles (such as automobiles, vans and trucks), based on the amount of \( W \) and the distance of detonation \( R \) [52,65].

In this research study, three types of surface burst explosive packs with 55, 275 and 555 kg of trinitrotoluene (TNT) are considered and can be reasonably assumed to be carried by an automobile, a van or a truck, respectively. The stand-off distance is also considered to modify in each blast scenario, in order to find the minimum required SPD, using the reliability analysis. It should be noted that human-made explosions generally occur on the vicinity of the ground surface. Due to this closeness, an immediate interaction initiates between the blast wave and the ground, which forms the hemispherical surface burst [66]. The incident waves are quickly reflected from the ground surface and lead to higher pressure values [67]. Based on [38,52,66,68–70], the parameters of the hemispherical surface burst (reflected pressure \( P_r \) and the positive time duration \( t_d \)) can be defined using the conventional relationships for free air burst, by replacing \( W \) with the effective charge weight \( W_{\text{eff}} = 1.8 \times W \). Finally, the blast load time history is defined based on the calculated surface burst parameters and is considered as a simplified equivalent triangular pulse, for all the FE modelled configurations. For the sake of conciseness and to avoid lengthening, no major details about definition of time history of blast loading are reported in this paper. More details can be found in [52,57].

2.3. Damage Evaluation Assessment Based on Damage Index Criterion

To numerically assess the expected damage of blast loaded steel columns after explosion, the damage index (DI) based on residual axial carrying capacity is taken into account in this study. According to Shi et al. [25], this index is given by:

\[
\text{DI} = 1 - \frac{P_{\text{residual}}}{P_{\text{initial}}}
\]  

where \( P_{\text{residual}} \) is the post-blast residual axial capacity of the damaged column and \( P_{\text{initial}} \) is the maximum axial load-carrying capacity of the undamaged column. The degrees of damage are thus categorized into four levels [25], namely corresponding to:

(a) \( \text{DI} = 0–0.2 \) low damage;
(b) \( \text{DI} = 0.2–0.5 \) medium damage;
(c) \( \text{DI} = 0.5–0.8 \) high damage;
(d) \( \text{DI} = 0.8–1.0 \) collapse.

It should be noted that for vertical load bearing components belonging to high-class buildings that are sensitive to lateral deformations and must be designed for maximum lateral ductility ratio \( \xi \), no relevant damage is allowed and consequently DI must be selected in such a way that this limitation is satisfied. From a computational point of view, several calculation steps must be generally carried out to find the expected \( P_{\text{residual}} \) value. The sequence of required steps, however, is not reported in this paper for the sake of conciseness. Additional details can be found in [52,57]. In blast-resistant design of structures, it is often stated that the damage caused in a structure due to blast loads would be reduced if the structure is well designed against seismic loadings. This is not true in all cases and it should not be assumed that a structure designed to withstand seismic
loads is sufficient to resist the prescribed blast loading or prevent subsequent progressive collapse. Despite the similarities between seismic and blast loadings, the global response of buildings subjected to blast loading is not usually critical. In the other words, for a structure that is affected by an explosion, only its critical members (i.e., closer to detonation) are individually assessed and designed by means of different methods (SDOF and FE models) and damage criteria (support rotation and damage index), while for building structures under the effects of earthquake loadings, the global deformations (inter-story drifts) must be evaluated based on the desired performance level (life safety) as the most important response parameter [71,72]. In the design of structures under seismic and blast loading, the desirable features of design—that is, the provision for ductility in member response and increasing the ability to redistribute extreme loads to lesser-loaded elements—must be satisfied.

3. Random Variables and Reliability Analysis Using MCS

3.1. Random Variables

The variability of blast loading parameters is one of the key variables of the problem explored herein. A number of documents [34,36,73] have reported constant coefficient of variation (COV) values for the variability of blast loads at various scaled distances. On the other hand, the observed statistics obtained from blast tests and empirical formulations confirm the basic variability. To overcome this major limit, additional studies were performed in [35,37,73]. Among others, the proposals by Hao et al. [35] and Netherton and Stewart [37] are of general application and thus often used in the reliability analysis of blast loaded structures. Although the cited strategies are different, the shared feature is the blast load variability, which is expressed in terms of Z. Furthermore, the same strategies are validated for a wide range of scaled distance values (0.24 m/kg\(^{1/3}\) ≤ Z ≤ 40 m/kg\(^{1/3}\) in [35] and 0.59 m/kg\(^{1/3}\) ≤ Z ≤ 40 m/kg\(^{1/3}\) in [37]). As a final result of the formulations provided in [35] and [37], for a blast scenario (with specified charge weight and stand-off distance) the mean, standard deviation (σ) and COV of wave parameters can be estimated as a function of Z. In this paper, \(P_r\) and \(t_d\) are selected as random variables for blast loading. It is also assumed that the uncertainties are defined based on [35], that is:

\[
\log P_r(\text{mean}) = 3.651 - 3.018 \times \log Z + 0.1967 \times (\log Z)^2 + 0.8873 \times (\log Z)^3 - 0.3795 \times (\log Z)^4
\]

(3)

\[
\log \sigma_{P_r} = 3.03 - 3.533 \times \log Z + 0.4534 \times (\log Z)^2 + 0.3248 \times (\log Z)^3 + 0.07896 \times (\log Z)^4
\]

(4)

\[
\log \text{COV}_{P_r} = -0.6239 - 0.5726 \times \log Z + 0.3203 \times (\log Z)^2 - 0.3538 \times (\log Z)^3 + 0.2973 \times (\log Z)^4
\]

(5)

\[
\log \left(\frac{t_d(\text{mean})}{w^{1/3}}\right) = -0.00307 + 1.2186 \times \log Z - 0.5207 \times (\log Z)^2 - 0.2835 \times (\log Z)^3 + 0.2132 \times (\log Z)^4
\]

(6)

\[
\log \sigma_{t_d/w^{1/3}} = -0.8433 + 1.0982 \times \log Z - 0.8127 \times (\log Z)^2 + 0.4214 \times (\log Z)^3 - 0.1046 \times (\log Z)^4
\]

(7)

\[
\log \text{COV}_{t_d/w^{1/3}} = -0.8411 - 0.1186 \times \log Z - 0.2868 \times (\log Z)^2 + 0.6955 \times (\log Z)^3 - 0.3141 \times (\log Z)^4
\]

(8)

Equations (3)–(8), in more detail, represent the statistical characteristics (mean, σ and COV) of the \(P_r\) and \(t_d\) variables, as a function of Z, in the range of 0.24 m/kg\(^{1/3}\) ≤ Z ≤ 40 m/kg\(^{1/3}\). It should be noted that the log in these equations is the logarithm to the base 10. As reported in [35], the proposed formulas are valid only for an open field explosion and large enough flat reflection surface. For a complex explosion scenario, such as an explosion in a complex city environment, more significant variations are expected because of blast wave interactions with surrounding structures.
It should be noted that \( t_d \) is the positive time duration of an idealized triangular blast loading history with sufficient accuracy instead an exponentially decayed loading history of a real explosion. The assumption of using triangular pressure-time history for blast loading originates from past research studies, such as [35,37,38,42,43,55,74–79]. There, the variation of the waveform coefficient for the positive pressure phase has been generally disregarded for the reliability analysis, due to lack of information. This issue depends on blast load databanks that have been used to propose analytical formulas to calculate the variation of blast load parameters as functions of scaled-distance. Among others, the parameter corresponding to the waveform coefficient has been considered probabilistic in [48,73], but the intended scaled distance was set between 1.62 and 2.78 m/\( kg^{1/3} \), and an explicit relation was not presented for the calculation of statistical properties (i.e., mean and standard deviation) of the waveform coefficient based on scaled distance. Although the linear assumption of blast load imposes some unwanted approximation in the problem [35], such an assumption might cause an error up to 10% for the final results. In this paper, following former dedicated research [35,37,38,42,43,55,74–79], a linear function is thus used to define the input blast.

Normal probability density function (PDF) is used for all input random parameters including loading parameters (\( P_r \) and \( t_d \)) and steel material properties (\( F_y \) and \( E_s \)), see Table 1 [35,42,80–82].

| Random Variable | Mean            | \( \sigma \)    | COV  | PDF   |
|-----------------|-----------------|-----------------|------|-------|
| \( P_r \)       | Equation (3)    | Equation (4)    | Equation (5) | Normal |
| \( t_d \)       | Equation (6)    | Equation (7)    | Equation (8) | Normal |
| \( F_y \)       | 240 \( \times \) 1.15 MPa | 16.56 MPa     | 0.06  | Normal |
| \( E_s \)       | 210 GPa         | 8.40 GPa       | 0.04  | Normal |

### 3.2. MCS Method

The MCS method is a well-known technique for estimating statistical properties of structural systems under stochastic uncertainties of input parameters [83,84] and is used in this paper to carry out the reliability analyses. MCS is one of the simplest and relatively most accurate methods which provides a feasible way to determine the reliability index, where the limit state function is more complicated. Most of the literature studies on the reliability of structures under blast loading have been performed using MCS. The probability of failure based on MCS equals to \( P_f = N_f/N \), where \( N \) is the number of total simulations and \( N_f \) is the number of trials for which limit state function, \( g(X) = r-q \), falls in the failure region or has negative value. In the definition of the state function, \( X \) is the vector of input random variables, \( r \) is the capacity or resistance, \( q \) is the demand or loading. The probability of failure can also be written as follows:

\[
P_f = P(g(X) \leq 0) = \int_{g(X) \leq 0} f_X(X) \, dX = \frac{\sum_{i=1}^{N} I_F(X_i)}{N} \tag{9}
\]

where \( f_X(X) \) is the joint probability density function and \( I_F \) is the failure indicator which equals 1 if \( g(X) \leq 0 \) and 0 if \( g(X) > 0 \).

The accuracy and precision of MCS in damage estimation directly depends on the \( N \) value. The higher the \( N \) value, the more precise the MCS. On the other hand, by increasing the number of simulations, the computational effort is also increased, which is the main disadvantage of the MCS method. In this regard, there are many procedures in the literature to find the minimum number of iterations required for MCS for a certain level of accuracy. The equation proposed by Broding et al. [85] is taken into account in this paper:

\[
N > \frac{-\ln(1 - C_L)}{P_f} \tag{10}
\]
where \( N \) is the minimum number of required random samples, \( P_f \) is the probability of failure and \( C_L \) is the confidence level. In this paper, the value \( N = 300 \) is taken into account for reliability analyses, which corresponds to 95% confidence \((C_L = 0.95)\) and 0.99 reliability \((P_f = 0.01)\).

4. Methodology of Calculating SSD Using Reliability

4.1. SSD Definition

SPD is defined as the minimum required stand-off distance where the probability of low damage based on Equation (2) is at least 95% \([86–88]\) or the damage probability is lower than an acceptance criterion 5%. Figure 3 shows schematically an instance of probability of low damage diagram for a given charge weight, based on stand-off distance, that can be obtained from the results of reliability analysis for any blast loaded member. The concept in Figure 3 is shown for the specific case of probability of low damage 95%. The philosophy is that the structure object of analysis is examined for different blast scenarios (under constant charge weight and a variable stand-off value) and the probability of low damage in each case is calculated and drawn in Figure 3. In the other words, each point in Figure 3 corresponds to probability of low damage for the selected configuration under a blast scenario.

![Figure 3. The concept of calculating SPD.](image)

The desired output is obtained by a complete probabilistic analysis using MCS with 300 different simulations. The final result agrees with Figure 3 and is the basis for the SPD determination. This is in fact calculated as the stand-off distance corresponding to the intersection point between the diagram in Figure 3 and the probability of low damage 0.95. Once the SPD is known, the SSD can be easily determined, given that SSD = SPD/W^{1/3}.

4.2. Application of Reliability Analysis Based on MCS in Calculating SSD

Key steps to perform the SSD by implementing the concept of reliability analysis with MCS method and FE method (based on LS-Dyna software simulations) are summarized in this section. The full calculation process takes advantage of a set of LS-PrePost, MATLAB, LS-DYNA and C# coding for each FE model, thus importing the models into LS-DYNA.
and extracting and post-processing the results of interest. As shown in Figure 4, the general procedure can be basically described as follows:

1. Definition of boundary conditions, section properties and length for the examined steel column.
2. Generation of the initial LS-DYNA model (input file) for the considered steel column. At this stage, hypothetical (average) values are used for input random parameters. The same values are then updated in the following calculation steps, based on the real values of generated samples, for each random parameter. The aim of step 2 is only to create a .k file format for the column that will be object of the probabilistic analysis.
3. Selection of a blast scenario, by defining corresponding values for charge weight and stand-off distance.
4. Calculation of the mean values and standard deviations for the input random variables. In this paper, the attention is focused on blast load parameters (\(P_r\) and \(t_d\)) and material properties (\(F_y\) and \(E_s\)), according to Table 1.
5. Choice of appropriate probability density functions for the selected input random variables.
6. Generation of random variables (MATLAB code) according to the selected PDF (step 5).
7. Update of the initially generated LS-DYNA model (input file, see step 2), for the number of generated random variables (step 6), using MATLAB.
8. Analysis of all the FE models (by automatically running LS-Dyna software with C# coding) and extracting all the damage indices (MATLAB).
9. Derivation of histogram, PDF and Cumulative Distribution Function (CDF) for the calculated DI (from step 8).
10. Calculation of the probability of low damage, or \(P[DI \leq 0.2]\).
11. And in conclusion, a double check must be necessarily carried out, given that:
   - If the probability of low damage from step 10 is approximately 95%, the selected stand-off distance (step 3) coincides with SPD and consequently the required SSD can be calculated.
   - Otherwise, if the probability of low damage is less or more than 95%, the selected stand-off distance (step 3) must be increased or decreased, respectively. The full algorithm must be thus repeated (from step 3), until the probability of low damage reaches 95%.

4.3. Verification of Reliability Analysis Based on MCS Using Beam Element Formulation

In order to verify the current MCS results based on beam element formulation, major outcomes from the reliability analyses presented in [52] are compared in this study. In more detail, the numerical results of two loading cases (Case 1 and Case 2) are considered, as obtained for a steel column with section type IPBv200, nominal length of 3.6 m and pinned ends. The column from [52] is made of ST37 steel, with density of 7850 kg/m³. Yield strength, elastic modulus, Poisson’s ratio and failure strain are set equal to 240 MPa, 210 GPa, 0.3 and 0.2 respectively. In Case 1, the column is subjected to \(W = 55\) kg of TNT and \(R = 6\) m. In Case 2, the explosive charge weight and the stand-off distance are set to 55 kg and 8 m. For both configurations, the number of simulations is set to 300. The comparison of past [52] and current numerical results is shown in Figure 5a,b, for Cases 1 and 2, respectively, in terms of CDFs for DI.
Comparison of the results of MCS based on beam (present study) and shell element types [52] for CDFs of DI:

(a) Case 1; (b) Case 2.

**Figure 5.** Comparison of the results of MCS based on beam (present study) and shell element types [52] for CDFs of DI: (a) Case 1; (b) Case 2.

**Figure 4.** Procedures for SSD derivation based on structural reliability approach.
Based on Figure 5a,b, it can be clearly noticed that there is a rather close correlation between the collected results, even in the presence of different accuracy levels for the FE models in use (beam and shell elements, respectively). For Case 1, according to Figure 5a, the probabilities of low damage (DI < 0.2) are found to be 0.25 (present study) and 0.22 [52], with a scatter of 12%. In Case 2, see Figure 5b, the probabilities of low damage (DI < 0.2) are calculated at 0.90 (present study) and 0.93 [52], respectively, with a 3.22% scatter that further confirms the good agreement between the compared MCS results. In order to better clarify the performance of beam elements in probabilistic analysis, the required analysis durations for reliability analyses of the so-called Case 1 with beam and shell element types are thus presented in this paper. For beam elements, the typical required time was approximately 0.90 h for 300 MCS iterations. For shell elements [52], the required time was in the order of 30 h for the same number of iterations (that is, 33.33 times higher), which shows that implementing beam elements speeds up the procedure, especially in finding SPD and SSD values which need many separate reliability analyses.

### 4.4. Selected Columns

Given the potential of beam element formulation, a set of H-section steel columns with different geometrical properties in cross sections (IPB180 to IPB500) and lengths (2.8, 3.2, 3.6 and 4.0 m) are considered in the FE parametric investigation. The reference cross-sectional parameters are shown in Table 2, where $A_g$ is the cross-sectional area, $I_x$ is the moment of inertia about the strong axis (x-axis), $I_y$ is the moment of inertia about the weak axis (y-axis).

| Identification | b (mm) | h (mm) | s (mm) | t (mm) | $A_g$ (cm$^2$) | $I_x$ (cm$^4$) | $I_y$ (cm$^4$) |
|----------------|-------|-------|-------|-------|---------------|---------------|---------------|
| IPB 180        | 180   | 180   | 8.5   | 14.0  | 65.3          | 3831          | 1363          |
| IPB 220        | 220   | 220   | 9.5   | 16.0  | 91.0          | 8091          | 2843          |
| IPB 260        | 260   | 260   | 10.0  | 17.5  | 118.4         | 14,920        | 5135          |
| IPB 300        | 300   | 300   | 11.0  | 19.0  | 149.1         | 25,170        | 8563          |
| IPB 340        | 300   | 340   | 12.0  | 21.5  | 170.9         | 36,660        | 9690          |
| IPB 400        | 300   | 400   | 13.5  | 24.0  | 197.8         | 57,680        | 10,820        |
| IPB 500        | 300   | 500   | 14.5  | 28.0  | 238.6         | 107,200       | 12,620        |

### 5. Results and Discussions

#### 5.1. Curves of Probability of Low Damage

The curves of probability of low damage are obtained in this paper for all the steel sections presented in Table 2 via reliability analysis, for both the pinned and fixed ends under different blast scenarios (with TNT charges of 55, 275 and 555 kg). For example, Figure 6a–c illustrate the numerical curves for IPB220 with pinned ends under explosive charge weights of 55, 275 and 555 kg, respectively. Each plot corresponds to a column with a specified length and explosive charge. Furthermore, it consists of some observed points that are obtained from reliability analyses. Each observed point and its probability of low damage is in fact the result of a reliability analysis based on the MCS method with 300 simulations. In total, 15,900 simulations were performed to extract Figure 6a–c, indicating the high amount of computational effort, which was around 47.4 h. Additionally, the normal CDFs have been fitted to the observed points for each case related to a specified column length, to convey a better understanding of presented concepts in Section 4 and also calculating the probability of low damage for points other than the observed points, if necessary. Given that the stand-off distance corresponding to the 95% probability of low damage is considered for finding safe distance (see Figure 4), then the fitting operation was used to find the stand-off distance corresponding to exactly 95% probability of low damage. In this case, lower tails are not important and will not affect the calculation and extraction of SPD and SSD.
Figure 6. Curves of probability of low damage for IPB220 with pinned ends and different lengths subjected to: (a) 55, (b) 275 and (c) 555 kg of TNT.

According to Figure 6c, the SPD value for IPB220 with pinned ends and 3.6 m of length, subjected to 555 kg of TNT, is approximately calculated as 20.2 m by considering the 95% probability of low damage as a criterion and using orange arrows connected to normal fitted CDF for L = 3.6 m which eventually shows the value of SPD on the horizontal axis. As can be estimated from the figure, by changing the criterion from 95% to 99%, the SPD increases to 21.0 m. The important aspect, in this regard, is that the exclusive calculation of the SPD value for a column is not a sufficient way to provide protection against catastrophic events or major releases. In other words, finding the SPD value of 21.0 m by selecting 99% probability of low damage instead of 20.2 m (with 95% probability) does not mean that the safety of the examined steel column (or generally the whole structure) is ensured at this distance, without considering additional special arrangements. As such, the SPD values can be thus used as a valuable guidance to design and provide special arrangements around the building (such as appropriate access control and security guards), so as to reduce the frequency and/or the possible consequences to an acceptable level. The reliable prediction of adequate distances or separation zones around the building is thus one of the fundamental considerations for safe layout and can be designed according to SPD values. In some cases, it is worth mentioning that providing SPD for a structure to protect from all possible events is not practicable and this is especially the case in urban places,
due to the lack of sufficient space between buildings and access roads. The assessment of the frequency of the expected event and its potential consequences is thus necessary to understand which risks can be reasonably mitigated by an SPD. For cases in which the obtained SPD value is too large, of course, additional mitigating or prevention measures should be considered. In a nutshell, the 95% criterion is internationally recognized to represent a rational choice for finding practical SPD that causes no serious damage for the structure (if special arrangements are provided) and the designer’s judgment along with SPD values should lead to better decisions for ensuring safety of the structure under such events.

Similarly, Figure 7a–c present the curves of probability of low damage for IPB220 with fixed ends, subjected to explosive charge weights 55, 275 and 555 kg, respectively. As also explained in Section 4, using the obtained curves, the required SPD and the corresponding SSD can be calculated for each column by using orange arrows connected to each fitted curve. For instance, as Figure 6c reveals, the SPD values for IPB220 with different column lengths (2.8, 3.2, 3.6 and 4.0 m) and pinned ends are calculated in 16.9, 18.8, 20.2 and 21.2 m, respectively. Consequently, the SSD for lengths 2.8, 3.2, 3.6 and 4.0 m (and an explosive charge weight of 555 kg of TNT) are 2.06, 2.29, 2.46 and 2.58 m/kg$^{1/3}$, respectively.

Figure 7. Curves of probability of low damage for IPB220 with fixed ends and different s lengths, subjected to: (a) 55, (b) 275 and (c) 555 kg of TNT.
As shown, when increasing the column length, the SSD also increases. The reason is that the longer the column length (and thus slenderness), the more it is exposed to premature buckling which reduces the overall residual axial load capacity and further results in more severe damage and thus higher SPD value. In the case of fixed ends, according to Figure 7c, the SPD values are obtained in 11.8, 13.0, 13.9 and 15.0 m, which correspond to SSD values of 1.44, 1.58, 1.69 and 1.83 m/kg$^{1/3}$ for 555 kg of TNT and column lengths of 2.8, 3.2, 3.6 and 4.0 m, respectively. As evidenced, by changing the support condition from pinned to fixed ends, the calculated SSD decreases. The actual boundary condition has thus a significant effect on the final performances and results. Moreover, considering the fact that the end conditions for real columns are neither fully pinned nor fixed, it is preferable for designers to take into account an actual value between the two limit conditions of perfectly pinned or fixed column models, which ultimately leads to choosing an SPD in between [89].

It should be noted that the variability of stand-off distance is highly dependent on the position of the explosive, given that the location of a terrorist device is not a certain parameter. When the target is known, the minimum stand-off distance from a facility (building, bridge, etc.) is obtained from the knowledge of the site (roads, parking, etc.), the access control (security gates, bollards, etc.) and the perimeter security [78]. Generally, for a critical building that may represent a target for terrorist attacks with variable and portable explosive weights (i.e., by human and different vehicles), the minimum stand-off distance can be easily found using the proposed strategy. Such a minimum stand-off distance can be thus used to provide appropriate access control and security guards around the building, thus ensuring that the risk of damage for the structural members in the first stage and the progressive collapse can be reduced.

Further, the residual axial load carrying capacity of a column (which is used to obtain DI) alternates between minimum (zero) and maximum ($P_{\text{initial}}$) values. This variation depends on geometrical properties and boundaries of the column, as well as on some uncertainties associated with blast loading and material properties. For all the cases in which the SPD is calculated, due to the fact that 95% probability of low damage is considered as decision criterion, the residual capacity of a given column under a selected blast scenario is expected to approach $P_{\text{initial}}$, or equivalently, the DI values are expected to approach zero. To better clarify the given explanations, Figure 8 shows the DI histograms obtained from MCS for a given IPB260 steel column with length of 3.6 m and pinned ends, subjected to 55, 275 and 555 kg of TNT. In all these cases, the probabilities of low damage are approximately calculated as 0.95, and, consequently, the proposed stand-off distances on the top of each figure are related to SPD value for the selected charge weights. As Figure 8 reveals, in all cases, the frequency of the DI obtained from MCS tends to low DI values (almost between DI = 0 and DI = 0.5), while the possibility of high damage (0.5 < DI < 0.8) and collapse (DI > 0.8) is really rare.

5.2. Empirical Relationship for Calculating SSD

The curves of probability of low damage were extracted similar to the approach presented in Section 5.1 to find the SSD values for all selected configurations (Table 2). Both pinned and fixed end conditions are examined, including different column lengths and explosive charge weights (55, 275 and 555 kg of TNT). A large number of FE simulations (approximately 252,000) were conducted for reliability analyses based on MCS, which took nearly 756 h of run time. The collected data were further investigated to find a practical relationship which could support designers in the predicting the SSD for steel columns under blast loads. By examining the results after a lot of trial-and-error process, it was finally found that the SSD can be expressed as:

$$SSD(W, P_{\text{initial}}) = \alpha_0 + \alpha_1 W + \alpha_2 P_{\text{initial}} + \alpha_3 W^2 + \alpha_4 W P_{\text{initial}} + \alpha_5 P_{\text{initial}}^2$$

(11)

where the parameters $\alpha_0$ to $\alpha_5$ are constant coefficients. The final values of these $\alpha_i$ coefficients, as well as the coefficient of determination ($R^2$) values, goodness of fit (GoF)
and root-mean-square error (RMSE), are shown in Table 3 for different columns, as obtained from curve fitting. It is clear that the $R^2$ values are higher than 97% for all the selected configurations, hence indicating a very satisfactory accuracy of the proposed formula for SSD predictions (usually, $R^2$ values higher than 80% are considered satisfactory).

![Figure 8. DI histograms, as obtained from MCS for IPB260 steel column with length of 3.6 m and pinned ends under: (a) 55, (b) 275 and (c) 555 kg of TNT.](image)

**Table 3.** Constant coefficients of Equation (11) and corresponding $R^2$, GoF and RMSE for each selected case (BC = boundary condition).

| BC   | Length (m) | $\alpha_0$ | $\alpha_1$ | $\alpha_2$ | $\alpha_3$ | $\alpha_4$ | $\alpha_5$ | $R^2$  | GoF  | RMSE  |
|------|------------|-------------|-------------|-------------|-------------|-------------|-------------|--------|------|-------|
| Pinned | 2.80       | 2.600       | +1.313 $\times 10^{-3}$ | $-4.101 \times 10^{-4}$ | $-1.351 \times 10^{-6}$ | $+3.199 \times 10^{-8}$ | $+1.502 \times 10^{-10}$ | 0.9943  | 0.0199 | 0.0364 |
|      | 3.20       | 2.765       | +1.383 $\times 10^{-3}$ | $-4.219 \times 10^{-4}$ | $-1.528 \times 10^{-6}$ | $+5.498 \times 10^{-9}$ | $+1.356 \times 10^{-10}$ | 0.9958  | 0.0177 | 0.0343 |
|      | 3.60       | 2.959       | +1.269 $\times 10^{-3}$ | $-4.348 \times 10^{-4}$ | $-1.527 \times 10^{-6}$ | $+4.701 \times 10^{-9}$ | $+9.666 \times 10^{-10}$ | 0.9930  | 0.0338 | 0.0475 |
|      | 4.00       | 3.056       | +1.173 $\times 10^{-3}$ | $-4.018 \times 10^{-4}$ | $-1.399 \times 10^{-6}$ | $+6.757 \times 10^{-9}$ | $-2.381 \times 10^{-10}$ | 0.9945  | 0.0287 | 0.0437 |
| Fixed | 2.80       | 1.852       | +6.884 $\times 10^{-4}$ | $-2.723 \times 10^{-4}$ | $-5.899 \times 10^{-7}$ | $+4.833 \times 10^{-9}$ | $+9.599 \times 10^{-10}$ | 0.9825  | 0.0298 | 0.0446 |
|      | 3.20       | 2.039       | +5.398 $\times 10^{-4}$ | $-2.825 \times 10^{-4}$ | $-3.748 \times 10^{-7}$ | $-1.978 \times 10^{-9}$ | $+9.041 \times 10^{-10}$ | 0.9739  | 0.0513 | 0.0585 |
|      | 3.60       | 2.105       | +1.046 $\times 10^{-3}$ | $-2.847 \times 10^{-4}$ | $-9.854 \times 10^{-7}$ | $-1.322 \times 10^{-9}$ | $+7.141 \times 10^{-10}$ | 0.9771  | 0.0538 | 0.0599 |
|      | 4.00       | 2.266       | +6.718 $\times 10^{-4}$ | $-2.705 \times 10^{-4}$ | $-5.376 \times 10^{-7}$ | $+1.577 \times 10^{-9}$ | $+1.872 \times 10^{-10}$ | 0.9782  | 0.0562 | 0.0612 |
There are two conventional ways to calculate $P_{\text{initial}}$: one based on FE modelling and another based on the empirical relationships that are presented in several regulations. In this study, the second method is used, which is easier to apply, is efficient and can be extended to each column, without the need of any complex calculation. The final result is that, even disregarding sophisticated FE methods, the $P_{\text{initial}}$ prediction can be used in Equation (11) and it can be consequently assessed (for a specific explosive charge weight) whether the column is in a safe condition or not. According to the regulations, in more detail, $P_{\text{initial}}$ for members under compression without slender elements can be calculated as:

$$P_{\text{initial}} = F_{\text{cr}} \times A_g$$

$$\begin{align*}
(k_\ell \frac{L}{r_g})_{\text{max}} &\leq 4.71 \sqrt{\frac{F_y}{F_{\text{cr}}}} &\Rightarrow F_{\text{cr}} = \left[0.658 \frac{F_y}{F_{\text{cr}}} \right] F_y \\
(k_\ell \frac{L}{r_g})_{\text{max}} &> 4.71 \sqrt{\frac{F_y}{F_{\text{cr}}}} &\Rightarrow F_{\text{cr}} = 0.877 F_e
\end{align*}$$

(12)

where $F_{\text{cr}}$ is the critical stress due to flexural buckling and $L$, $r_g$ and $k_\ell$ are, respectively, the column length, the radius of gyration and the effective length factor. For a column with pinned ends or fixed ends, it is assumed $k_\ell = 1$ or $k_\ell = 0.5$, respectively. Finally, $F_e$ is the elastic buckling stress which can be calculated as:

$$F_e = \frac{\pi^2 E_s}{(k_\ell \frac{L}{r_g})^2}$$

(13)

Figures 9 and 10 show the predicted SSD values and the corresponding fitted planes (according to Equation (11)) for pinned and fixed ends and for different column lengths. In these figures, the numerical data collected from reliability analyses for different steel configurations and blast scenarios are represented by 21 points which are used for curve fitting (Equation (11)).

![Figure 9](image-url)
Figure 9. SSD values for steel columns with pinned ends and different lengths: (a) $L = 2.8$ m, (b) $L = 3.2$ m, (c) $L = 3.6$ m and (d) $L = 4.0$ m.

Figure 10. Cont.
are the SPDs for W = 275 kg and W > 275 kg, respectively. Based on such an equation, the SPD for W values higher than 275 kg of TNT can be thus easily obtained, without the need for any further simulation. As an instance, the predicted SSD value for a steel column with IPB 220 section is calculated as 17.66 m, thus with a minimum percentage scatter (3.15%) compared to the expected value.

5.3. Verification of the Proposed Formula

The proposed analytical correlation for calculating the SSD was finally further discussed and verified. To this end, the numerical results from [52] were taken into account.

\[
\text{SSD}_{(W=275)} \cong \text{SSD}_{(W>275)}
\]

\[
\text{SSD}_{(W=275)} = \frac{\text{SPD}_{(W=275)} \times W^{1/3}}{P_{\text{ini}}}
\]

\[
\text{SSD}_{(W>275)} = \frac{\text{SPD}_{(W>275)} \times W^{1/3}}{P_{\text{ini}}}
\]

where SSD_{(W=275)} and SSD_{(W>275)} are the safe scaled distances for W = 275 kg and W > 275 kg of TNT, respectively. Similarly, SPD_{(W=275)} and SPD_{(W>275)} are the SPDs for W = 275 kg and W > 275 kg of TNT, respectively. Based on such an equation, the SPD for W values higher than 275 kg of TNT can be thus easily obtained, without the need for any further simulation. As an instance, the predicted SSD value for a steel column with IPB 220 section and length of 3.6 m is 2.22 and 2.15, as obtained for TNT explosive charge weights equal to 555 or 275 kg. This results in SPD values of 18.24 and 13.98 m, respectively. Using Equations (14) and (15), the SPD_{(W>275)} for the aforementioned column is calculated as 17.66 m, thus with a minimum percentage scatter (3.15%) compared to the expected value.
For a pinned steel column with IPBv200 cross section (ST37 steel) and a total length of 3.6 m, subjected to different charge weights (55, 275 and 555 kg of TNT), the SPD values in [52] were predicted to be 8, 15 and 19 m, thus resulting in SSD values of 2.10, 2.30 and 2.31 m/kg$^{1/3}$, respectively. The input steel yield stress, density, elastic modulus and Poisson’s ratio were set to 240 MPa, 7850 kg/m$^3$, 210 GPa and 0.3, respectively. Furthermore, the geometrical characteristics of the resisting section (i.e., b, h, s and t, see Table 2), were set to 206, 220, 15 and 25 mm, respectively. It should be noted that the IPBv200 cross section is different from the intended steel sections presented in Table 2.

In order to analytically predict the SSD value based on Equation (11), the initial axial capacity of the column must first be calculated. Based on Equations (12) and (13), such a value can be estimated as 2518 kN. Consequently, by using Equation (14) and the constant coefficients presented in Table 2 (pinned ends and column length of 3.6 m), the corresponding SSD are easily calculated for selected explosive charges. The related values of SSD and SPD from Equations (14) and (15), together with those obtained from the previous study [52], are thus compared in Table 4. As shown, the percentage scatter $\Delta$ is also calculated for each case, giving evidence of the accuracy of the proposed method.

### Table 4. Verification results of the proposed formula, with respect to previous study [52].

| W (kg of TNT) | SSD Value (m/kg$^{1/3}$) | SPD (m) |
|---------------|---------------------------|---------|
|               | Hadianfard et al. [52]    | Present Study | $\Delta$ (%) | Hadianfard et al. [52] | Present Study | $\Delta$ (%) |
| 55            | 2.10                      | 1.99     | 5.24         | 8                        | 7.57         | 5.37         |
| 275           | 2.30                      | 2.18     | 5.21         | 15                       | 14.17        | 5.53         |
| 555           | 2.31                      | 2.21     | 4.33         | 19                       | 18.16        | 4.42         |

As Table 4 reveals, there is in fact a rather close correlation between the current proposed formula for the SSD calculation and the past numerical study reported in [52]. SSD values obtained by Equation (11) were equal to 1.99, 2.18 and 2.21 m/kg$^{1/3}$, respectively, for explosive charge weights of 55, 275 and 555 kg, and thus corresponding to a negligible scatter (5.24%, 5.21% and 4.33%) compared to the SSD values from [52].

### 6. Calculation Examples

In conclusion, to emphasize the applicability and usefulness of the proposed relationship, some calculation examples are presented. The objective of these examples is to find the SPD and SSD of:

(i) A steel column with IPB 240 cross section and L = 3.4 m (Section 1), and
(ii) A box shape steel column with L = 3.6 m and given geometrical properties in Table 5 (Section 2).

### Table 5. Sectional properties of selected box section steel column for calculation examples.

| Identification | b (mm) | h (mm) | f (mm) | w(mm) | A (cm$^2$) | $I_x$ (cm$^4$) | $I_y$ (cm$^4$) |
|----------------|--------|--------|--------|--------|------------|---------------|---------------|
| BOX            | 300    | 300    | 19.6   | 6.2    | 149.9      | 24,986        | 15,799        |

Section 1 differs from the intended columns presented in Table 2. Its length of 3.4 m, in particular, is further modified and differs with considered lengths (i.e., 2.8, 3.2, 3.6 and 4.0 m) in the reliability analyses, in order to create a databank for the relationship proposal. Section 2 is selected from [57], in which its sectional properties about bending axis is the same as for a IPB300 steel column, while its cross-sectional shape is totally different. Again, the material yield stress, density, elastic modulus and Poisson’s ratio are set equal to 240 MPa, 7850 kg/m$^3$, 210 GPa and 0.3, respectively. Finally, Section 1 is subjected to six different explosive charge weights (55, 200, 275, 350, 555 and 1000 kg.
of TNT), while Section 2 is subjected to 275 kg of TNT, under the assumption of two idealized boundary conditions, (a) pinned and (b) fixed ends. The reason for selecting an explosive weight of 1000 kg of TNT, in this regard, is to verify the accuracy of the proposed Equations (14) and (15) for calculating the SPD and SSD for explosive charge weights higher than 555 kg of TNT.

To determine the SSD of the selected configurations, the proposed relationship (Equation (11)) and the methodology earlier presented are employed. The results are collected in Table 6, for both the pinned and fixed ends. It is worth mentioning that the SSD values calculated by Equation (11) are obtained by an interpolation approach. This means that, for a column with a length other than those reported in Figures 9 and 10, for both pinned and fixed end conditions, the interpolation method should be always used to calculate the corresponding SSD. For the present calculation example, the SSD values for column lengths of 3.2 and 3.6 m are thus first calculated by Equation (11) and then, using the interpolation, the required SSD values are estimated for the assigned column length of 3.4 m.

Table 6. SSD and SPD calculations with different methods MCS and proposed practical equations.

| Column | B.C | W (kg of TNT) | Equations | SSD (kg/m$^{1/3}$) | SPD (m) |
|--------|-----|--------------|-----------|---------------------|--------|
|        |     |              | 11        | Equation (14) | MCS | $\Delta_1$ (%) | $\Delta_2$ (%) | Equation (15) | MCS | $\Delta_1$ (%) | $\Delta_3$ (%) |
| IPB    | Pinned | 55          | –         | 2.039       | 0.63 | –              | 7.80          | –              | 7.75 | 0.64 | –              |
|        | 200   | 2.192       | –         | 2.077       | 5.24 | –              | –              | 12.82         | –              | 12.15 | 5.23 | –              |
|        | 275   | 2.244       | 2.214     | 1.34        | 1.33 | 14.59          | 14.59         | 14.40          | 1.30 | 1.30 | –              |
|        | 350   | 2.254       | 2.172     | 3.63        | 3.20 | 15.88          | 15.81         | 15.31          | 3.58 | 3.16 | –              |
|        | 555   | 2.274       | 2.265     | 0.39        | 0.93 | 18.69          | 18.44         | 18.61          | 0.43 | 0.91 | –              |
|        | 1000  | –           | 2.278     | 1.49        | –    | 22.44          | 22.78         | –              | 1.49 | –    | –              |
|        | Fixed | 55          | –         | 1.416       | 3.41 | –              | 5.58          | –              | 5.38 | 3.58 | –              |
|        | 200   | 1.532       | –         | 1.438       | 6.14 | –              | 8.96          | –              | 8.41 | 6.13 | –              |
|        | 275   | 1.587       | 1.533     | 3.40        | 3.40 | 10.32          | 10.32         | 9.97           | 3.39 | 3.39 | –              |
|        | 350   | 1.614       | 1.558     | 3.46        | 1.83 | 11.37          | 11.18         | 10.98          | 3.43 | 1.78 | –              |
|        | 555   | 1.646       | 1.657     | 0.66        | 4.22 | 13.53          | 13.04         | 13.62          | 0.66 | 4.26 | –              |
|        | 1000  | –           | 1.598     | –           | 2.92 | –              | 15.87         | 15.98          | –    | 0.69 | –              |
| BOX    | Pinned | 275         | 1.874     | 1.874       | 3.36 | 12.18          | 12.18         | 11.78          | 3.28 | 3.28 | –              |
|        | Fixed  | 275         | 1.386     | 1.396       | 0.71 | 0.71           | 9.01          | 9.01           | 9.08 | 0.77 | 0.77           |

From Table 6, see Section 1, it is possible to notice that the proposed equation is able to provide a good level of accuracy for the estimation of the expected SSD under different explosive charge weights. Such an outcome is confirmed by the calculated percentage scatters, obtained between Equation (11) and MCS as $\Delta_1$, and between Equation (14) and a MCS as $\Delta_2$, and between Equation (15) and MCS as $\Delta_3$. It should be noted that the symbol dash (–) in Table 6 shows that input value of W is out of range for corresponding equation. Furthermore, for Section 2, it can be seen that the proposed relationship accurately predicts the required SPD and SSD values, in comparison to the FE-based MCS results. This is also consistent with the results presented in [57], where for steel columns with different cross-sectional shapes (but similar section properties) subjected to the same loading/boundary conditions, it was proved that the cross section shape has mostly null effects on the global response. In case of pinned ends, in more detail, the cross-sectional shape has little effect on the response of a given column, while in case of fixed ends the results may change up to 20% [57].

In this paper, the results obtained for Section 2 show that, for a non H-shape steel column that can be equaled to an H-section (within the examined range and with the
same loading/boundary conditions), the proposed formula can be used with accuracy to determine the SPD and SSD parameters. It should be kept in mind, however, that the proposed relationship is generally based on interpolation within the range of the intended columns. In general, it is hence recognized that the use of the proposed formula for other steel columns can provide a preliminary estimation of the required SPD and SSD values, but the accuracy of these results should be examined through engineering judgment and further investigations.

It is also clear, in this regard, that considering the high computational cost of the rigorous approach (almost 0.9 h for 300 simulations, and almost 4.5 h for each curve of probability of low damage, consisting of 5 points), the proposed approximate relationships can be efficiently used to obtain practical and reliable estimates.

The illustrative calculation examples, in conclusion, proved that the proposed formula is capable of properly interpolating the available data, and thus finding the SSD of various types of columns, which may differ in length and/or cross-sectional properties. Furthermore, such a relationship could be further extended to find the SSD of blast loaded steel columns with semi-fixed boundary conditions. Recently, a research study was in fact reported in [89] to investigate the effect of semi-fixed supports on the response of flexural members under impact loads. The equivalent SDOF system was used and the transformation factors including load, mass, stiffness and ultimate resistance factors were obtained for different fixity values in the elastic, elastic–plastic and plastic regions. It was thus shown that the semi-fixed condition can severely affect the blast response of a given column, compared to the two ideal assumptions of fully pinned and fully fixed support conditions. Accordingly, it is recognized that the current research outcomes—based on the SSD results for two perfectly pinned and fixed conditions—can support the designer with their engineering judgment in the choice of the SSD value (in between two limit support conditions) which is closest to the real boundary condition.

7. Conclusions

Safe scaled distance (SSD) is of practical interest, especially for design purposes of structural elements or assemblies, in order to minimize the damage probability and consequently the risk of progressive collapse against terrorist attacks in congested urban areas. In this paper, an improved methodology based on reliability analysis and implementing the beam element formulation was presented for calculating the SSD and the safe protective distance (SPD) for steel beam columns subjected to blast loads. To obtain the probability of low damage, the Monte Carlo simulation (MCS) method was used, so as to account for the uncertainties of blast loading parameters and material properties. The proposed methodology was extended to steel columns with different cross sections (IPB180 to IPB500), lengths (2.8, 3.2, 3.6 and 4.0 m) and boundary conditions (pinned or fixed ends). The collected data were thus further investigated to find a practical relationship to predict the SSD of steel columns under blast loads. From the comparative discussion, the following conclusions were obtained:

• The results showed that the improved methodology, based on the beam element formulation, has good efficiency and accuracy in predicting the damage probability of blast loaded steel columns and further remarkably reduces the run time of probabilistic analyses.
• A practical relationship was proposed and verified against numerical studies in the literature, to relate the SSD of blast loaded steel columns to the initial axial capacity and explosive charge weight.
• The proposed equation has a very good agreement with FE results based on MCS, which indicates its very high level of accuracy in predicting the SSD and thus its efficiency in obtaining practical and reliable estimates.
• The results showed that for both pinned and fixed end conditions, by increasing the initial axial carrying capacity of a given column and the amount of explosive charge weight, the SSD decreases and increases, respectively. The variation of the explosive
charge weight, however, has minimum effects on the calculated SSD, compared to variations in the initial axial capacity of the column.

- The discussed results proved that upon changing the support condition from pinned to fixed ends, the corresponding SSD decreases significantly. This indicates that the actual boundary condition has substantial effects on the SSD and the designer should consequently select an SSD value between two perfectly pinned and fixed models to account for real support conditions.

- For explosive charge weights (W) higher than or equal to 275 kg of TNT, by keeping constant the initial axial capacity, the effects of W variations on SSD are almost negligible. In a nutshell, the SSD obtained for W = 275 kg of TNT can be rationally taken into account, with an acceptable level of accuracy, for W values higher than 275 kg of TNT ($SSD_{(W=275)} \approx SSD_{(W>275)}$).

- Similarly, the SPD of a given steel column subjected to explosive charge weights higher than or equal to 275 kg of TNT can be easily obtained by calculating the SPD for $W = 275$ kg of TNT using the proposed equation.

Author Contributions: Conceptualization, M.M., C.B., M.A.H. and A.B.; methodology, M.M., C.B., M.A.H. and A.B.; formal analysis, M.M., C.B., M.A.H. and A.B.; validation, M.M., C.B., M.A.H. and A.B.; writing—original draft preparation, M.M., C.B., M.A.H. and A.B.; writing—review and editing, M.M., C.B., M.A.H. and A.B.; visualization, M.M., C.B., M.A.H. and A.B.; supervision, C.B., M.A.H. and A.B. All authors have read and agreed to the published version of the manuscript.

Funding: This research received no external funding.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Supporting data will be made available upon request.

Acknowledgments: The authors wish to acknowledge and express their special thanks to Sina Malekpour and Fateme Hajari from Department of Civil and Environmental Engineering, Shiraz University of Technology, Shiraz, Iran.

Conflicts of Interest: The authors declare no conflict of interest.

Abbreviations

| Abbreviation | Description                        |
|--------------|------------------------------------|
| MCS          | Monte Carlo Simulation             |
| SPD          | Safe Protective Distance           |
| SSD          | Safe Scaled Distance               |
| FE           | Finite Element                     |
| RC           | Reinforced Concrete                |
| SDOF         | Single Degree of Freedom           |
| MDOF         | Multi Degree of Freedom            |
| DIF          | Dynamic Increase Factor            |
| DI           | Damage Index                       |
| GoF          | Goodness of Fit                    |
| RMSE         | Root-Mean-Square Error             |
| $R^2$        | Coefficient of determination       |
| PDF          | Probability Density Function       |
| CDF          | Cumulative Distribution Function   |
| COV          | Coefficient of Variation           |
| TNT          | Trinitrotoleuene                   |
| BC           | Boundary Condition                 |
| W            | Explosive charge weight            |
| $W_{eff}$    | Effective charge weight            |
| R            | Stand-off distance                 |
Z  Scaled distance
C and P  Constant coefficients of Cooper-Simonds relationship
k  Integration refinement factor
σ  Standard deviation
ε \text{t}  True stress
ε \text{t}  True strain
\dot{\varepsilon}  Strain rate
L_1  Deformed length of uniaxial tension member
L_0  Undeformed length of uniaxial tension member
P_r  Reflected pressure
P_{r(mean)}  Mean value of reflected pressure
σ_{Pr}  Standard deviation of reflected pressure
COV_{Pr}  Coefficient of variation of reflected pressure
t_{d}  Positive time duration
t_{d(mean)}  Mean value of positive time duration
σ_{td}  Standard deviation of positive time duration
COV_{td}  Coefficient of variation of positive time duration
P_{residual}  Post-blast residual axial capacity of the damaged column
P_{initial}  Maximum axial load-carrying capacity of the undamaged column
F_y  Yield stress
E_s  Modulus of elasticity
E_t  Slope of the bilinear stress strain curve in strain hardening region
P_f  Probability of failure
N_f  Number of trials for which limit state function falls in the failure region
N  Number of total simulations
X  Vector of input random variables
g(X)  Limit state function
r  Capacity
q  Demand
f_q(X)  Joint probability density function
I_F  Failure indicator
C_L  Confidence level
I_x  Moment of inertia about the strong axis
I_y  Moment of inertia about the weak axis
\alpha_0 to \alpha_5  Constant coefficients
F_{cr}  Critical stress due to flexural buckling of members without slender elements
A_g  Total cross-sectional area
L  Column length
r_g  Radius of gyration
k_e  Effective length factor
F_e  Elastic buckling stress
\Delta, \Delta_1, \Delta_2 and \Delta_3  Percentage scatters

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