Magnetoelectric effect in organic molecular solids

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The Magnetoelectric (ME) effect in solids is a prominent cross correlation phenomenon, in which the electric field ($E$) controls the magnetization ($M$) and the magnetic field ($H$) controls the electric polarization ($P$). A rich variety of ME effects and their potential in practical applications have been investigated so far within the transition-metal compounds. Here, we report a possible way to realize the ME effect in organic molecular solids, in which two molecules build a dimer unit aligned on a lattice site. The linear ME effect is predicted in a long-range ordered state of spins and electric dipoles, as well as in a disordered state. One key of the ME effect is a hidden ferroic order of the spin-charge composite object. We provide a new guiding principle of the ME effect in materials without transition-metal elements, which may lead to flexible and lightweight multifunctional materials.

The coupling between electric and magnetic polarizations in insulating solids has been accepted as exciting phenomena since the Curie’s early prediction of the ME effect1. A keystone in researches on the ME effect was brought by $\text{Cr}_2\text{O}_3$, for which a number of experimental and theoretical results have been reported since the discovery2–5. Interest in the ME effect has been recently revived6,7. This is ascribed to the several recent developments: i) large non-linear ME effects discovered in $\text{TbMnO}_3$ and other multiferroic materials with spin frustration8–14, ii) significant development of synthesis techniques for artificial ME composites, e.g. $\text{BaTiO}_3/\text{CoFe}_2\text{O}_4$15,16, and iii) a new theoretical framework for the ME polarizability, which is related to the axion electrodynamics, by which the ME tensor is evaluated qualitatively from first principles17,18. Almost all of the ME materials examined so far are transition-metal compounds, containing a vast treasury of magnetic and ferroelectric phenomena, allowing a coupling between the two.

Organic molecular solids are another class of materials, in which a wide variety of magnetic and dielectric phenomena emerges19. However, to the best of our knowledge, reports of the ME effect in organic molecular solids without transition-metal elements are limited so far. The fundamental unit of crystalline and electronic structures in this class of materials is the molecule rather than ion/atom in the transition-metal compounds. In particular, flexible $\pi$ molecular orbitals prescribe their magnetic and dielectric responses. Low-dimensional organic molecular solids, in which the molecular dimer units build a framework of the crystal lattice, have been ubiquitously targeted as multifunctional materials in recent decades. Series of tetramethyl-tetraphthaliafulvalene (TMTTF) and bis(ethylenedithio)tetraphthaliafulvalene (BEDT-TTF) compounds are the well-known examples. A rich variety of phenomena, e.g., superconductivity, quantum spin liquid state, ferroelectricity, and so on, have attracted considerable interest, and these have been ascribed to the molecular orbitals (MO) in dimer units20–27.

**Results**

**Symmetry consideration.** Here, we show that this dimer-type organic molecular solids provide an appropriate framework for the ME effect. We first present a symmetrical consideration for the ME effect in a simple one-dimensional chain model. Numerical calculations in a two-dimensional lattice modeling the $\kappa$-(BEDT-TTF) type organic molecular solids demonstrate that the linear ME effect emerges in a long-range ordered state of spins and electric dipoles owing to the electronic degree of freedom inside the molecular dimers. We identify that the essence of this phenomenon is attributable to a hidden ferroic order of the spin-charge composite object. The ME effect is also observed even in the spin and charge disordered state, in which the spin-charge composite ferroic order is realized. The present study of the ME effect provides a new strategy of material designs for a new type of multiferroic organic molecular solids.

Let us start from a simple example, a one-dimensional array of the molecular dimer units, as shown in Fig. 1, where the number of electrons are fixed to be equal to the number of the dimer units. This is a model for the one-dimensional chain in (TMTTF)$_2$X (X: monovalent anion). When a coupling between the two molecules in a dimer unit is strong enough, one electron (or hole) occupies a bonding (antibonding) MO in each dimer unit.

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This is identified as a Mott insulator, termed a dimer-Mott insulator, in the case in which the Coulombic interaction between electrons inside a dimer unit is larger than the bandwidth. Antiferromagnetic (AFM) alignment of electronic spins located at each dimer unit owing to the inter-dimer exchange interaction is a plausible magnetic structure (Fig. 1a) that is often realized.

Now, a degree of freedom inside a dimer unit is taken into account. A charge degree of freedom inside a dimer unit, i.e. the shape of the electronic charge cloud, is activated in the case in which the inter-dimer couplings overcome the gap between the bonding and antibonding MOs. Inequivalent charge distribution in the two molecules in a dimer unit induces a local electric dipole moment that is often called a “dimer dipole”. An alternate alignment of the dimer dipoles corresponding to the antiferroelectric (AFE) type order is one possible configuration on the chain due to a gain of the interaction between electrons in the nearest neighboring dimers. We show here that this spin and charge configuration, termed the multiferroic AFE + AFM order, shown in Fig. 1b has a key symmetry for the ME effects. This configuration is neither invariant by the space reversal operation (denoted by $s\mathcal{R}$) nor by the time reversal operation (denoted by $t\mathcal{R}$) as shown in Fig. 1c, while it is invariant by the spontaneous space-time reversal operation ($s\mathcal{R}t\mathcal{R}$) to the configuration in (b). Electric field ($E$) along the chain direction is applied on the polarized state in (b). Net magnetization ($M$) and electric polarization ($P$) are induced to be perpendicular and parallel to the chain, respectively.

Figure 1. Spin and charge configurations in a molecular dimer system where dimer units are arrayed on a one dimensional chain. Filled purple circles, shaded ovals, and thin red and blue arrows represent molecules, charge distributions, and spins, respectively. Shaded orange arrows represent electric dipole moments due to deformations of the charge clouds. Spins are aligned antiferromagnetically and are directed perpendicular to the chain. (a) An electrically non-polarized state, in which charge distributions in two molecules inside a dimer are equivalent. A corresponding one-dimensional chain composed of the TMTTF molecular dimers are presented in the upper panel, where the dotted circles denote the dimer units. (b) An electrically polarized state, in which charge distributions are polarized alternately, termed the multiferroic AFE + AFM state. (c) A spin and charge configuration obtained by applying the time reversal operation ($t\mathcal{R}$) or the space inversion operation ($s\mathcal{R}$) to the configuration in (b). (d) Electric field ($E$) along the chain direction is applied on the polarized state in (b). Net magnetization ($M$) and electric polarization ($P$) are induced to be perpendicular and parallel to the chain, respectively.
The above prediction from the symmetry consideration is embodied by the following microscopic picture. Let us set up the multiferroic AFE + AFM state in a chain, in which local magnetic moments are not fully polarized due to thermal and/or quantum fluctuations. Spins are assumed to be directed, for example along an axis perpendicular to the chain, due to a weak anisotropic interaction, such as the Dayaloshinskii-Moriya interaction. When electric field is applied along the chain, as shown in Fig. 1d, the electronic charge distributions in right-polarized and left-polarized dimers are no longer symmetric to each other under the space reversal operation. Since local electronic structures inside a dimer unit, in which spin and charge degrees of freedom are strongly entangled with each other, are inequivalent in the two kinds of dimers, amplitudes of the expectation values of local spins are different between the two dimers. As a result, the up- and down-spin polarizations are not canceled perfectly and a net magnetization appears. This is the spin-electronic contribution in the ME polarizability18.

**Microscopic model.** While the essence of the ME effect in the molecular dimer system is incorporated in this simple one-dimensional model, in reality such quantum spin chains often show the spin-Peierls states at low temperatures, rather than the AFM order31–34. Thus, we demonstrate the ME effect by numerical calculations in a realistic κ-(BEDT-TTF) type crystal lattice shown in Fig. 2a, where two-dimensional alignment of the dimer units prevents a paring of spins associated with the bond alternation. A minimal theoretical model for the molecular dimer systems showing the multiferroic AFE + AFM phase is known to be the Hamiltonian55,56 given by

$$\mathcal{H} = \sum_{\langle ij \rangle} S_i \cdot S_j - V \sum_{\langle ij \rangle} Q_i^x Q_j^x + \Gamma \sum_{i} Q_i^z - K \sum_{\langle ij \rangle} S_i Q_i^z Q_j^z,$$

(1)

where $S_i$ is a spin operator at $i$-th dimer unit with magnitude of 1/2. The charge degree of freedom inside a dimer unit is represented by the pseudo spin operator, $Q_i$, with magnitude of 1/2. The $x$ component, $Q_i^x = +1/2 (-1/2)$, represents an electrically polarized state, and the $z$ component, $Q_i^z = +1/2 (-1/2)$, represents a bonding (antibonding) MO state, where an electronic charge distribution is symmetric in a dimer unit. All interaction parameters are positive. The first term represents the conventional AFM Heisenberg interaction. The second and third terms, respectively, originate from the inter-dimer Coulomb interaction and the electron hopping between MOs inside the dimer units, and promotes and prevents the long-range order of the dimer dipoles. The last term represents a coupling between spins and dimer dipoles, and has a similarity to the Kugel-Khomskii type Hamiltonian for the orbital degenerated transition-metal compounds57. This model is derived from the generalized Hubbard-type model by the perturbational calculations, that are presented in the Supplemental Information (SI). In the following, $\Gamma/2$ corresponding to the intra-dimer hopping integral is taken as a unit of energy, which is approximately 0.3 eV for the typical κ-type BEDT-TTF compounds.

**ME effect.** A phase diagram on a plane of temperature ($T$) and the inter-dimer Coulomb interaction ($V$) calculated by the mean-field approximation introduced in SI is presented in Fig. 2a. In low temperatures, the two typical phases are confirmed; a multiferroic AFE + AFM ordered phase, where spins align antiferromagnetically and polarizations of the electronic clouds induce the canted AFE dimer-dipole order, as shown Fig. 2a, and an electrically non-polarized phase with AFM order, where the electronic clouds distribute symmetrically inside the dimer units. Spins are assumed to be directed along the $y$ axis due to a weak anisotropic interaction which is not included in the model explicitly. We focus on the multiferroic AFE + AFM ordered phase. Realizations of this phase were suggested experimentally in the BEDT-TTF compounds22,23.

A magnetization, an electric polarization, and ME response coefficients are calculated in finite $T$. An ME response coefficient, $\alpha_{\mu\nu} = dM_\mu / dE_\nu \bigg|_{E=0}$, is presented in Fig. 2b. In the parameter sets adopted in the numerical calculations (the dotted line in Fig. 2a), the AFE-type dipole order, characterized by an order parameter $P_{AF}$, occurs at a much higher temperature than the Néel temperature ($T_N$), as presented in Fig. 2c. It is shown that $\alpha_{\mu\nu}$ emerges below $T_N$ and disappears toward the zero temperature. This temperature dependence almost traces the magnetic fluctuation, shown in Fig. 2d, where a product of the magnetic susceptibility ($\chi_M$) and the AFE order parameter ($M_{AF}$) is plotted, indicating that the fluctuation is responsible for the ME effect as mentioned above. A large anisotropy in the tensor components of $\alpha$ is seen; there is no ME response when $E$ is parallel to the $y$ axis, because the electronic clouds for the up- and down-spins are equivalent even under the electric field. That is, $\alpha_{xy}$ is only finite in these spin and charge configurations. Although the ordered spins are assumed to be directed along the $y$ axis in the present calculation, the tensor components of $\alpha_{\mu\nu}$ emerge in a similar manner in the case where spins in the AFM phase are directed along other directions. A linearity of the induced $M$ with respect to $E$ expected from the symmetry consideration is obtained as shown in Fig. 2e. A schematic spin and charge configuration under the electric field applied to the $x$ axis is shown in Fig. 2f. We have checked that the inverse ME response coefficient, $\pi_{\mu\nu} = dP_\mu / dH_\nu \bigg|_{E=0}$, shows the same temperature dependence with $\alpha$. Since the magnetic field perpendicular to the spin direction does not break an equivalence of the two kinds of the polarized dimers, $\pi_{xy}$ is only finite.

**Spin-charge composite order.** So far, our discussion of the ME effect has been restricted in the multiferroic AFE + AFM ordered state, where the equivalence of the up- and down-spin sublattices or that of the two kinds of dimer-dipole sublattices is broken by the external fields. The necessary condition of the ME effect is generalized by introducing the composite operator of the spin and charge degrees of freedom defined by $\mathbf{T}_i = \sum_j 2p_i^z S_j$, termed the spin-charge composite operator, in which $\mathbf{p}$ is a local electric dipole moment at $i$-th dimer. A local dipole moment $\mathbf{p}$ is represented by $p_i^x = p_i^y = Q_i^x$ for the A dimers and $-p_i^x = p_i^y = Q_i^x$ for the B dimers, respectively, where the A and B dimers are defined in Fig. 2a. From the viewpoint of the multipole
moment, the spin distribution of this object is reduced to the magnetic dipole, magnetic quadrapole, and toroidal moments, as shown in Fig. 3, and the charge distribution is reduced to the electric dipole and electric quadrapole moments. This operator changes its sign by the space reversal operation, \( \mathcal{s} \), as well as by the time reversal one, \( \mathcal{t} \), but it is invariant by the simultaneous operation of \( \mathcal{s} \) and \( \mathcal{t} \). We show in the following that the ferroic order of \( \mathcal{U}_i \), i.e.,

\[
\tau = \sum_N \mathcal{U}_i
\]

with the number of dimers \( N \), gives rise to the ME effect, even with neither the AFM order nor the AFE order. Temperature dependence of \( \tau \) in the case of the multiferroic AFE + AFM state introduced above is presented in Fig. 2d, in which \( \sum \mathcal{S}_i \mathcal{S}_i \) in \( \tau \) is finite reflecting the symmetry of the charge and spin configuration in this phase.

In order to demonstrate this concept of the spin-charge composite order, we set up a model for the molecular dimer system where quenched randomness is introduced. This is modeled by randomly directed local electric field, \( h_i \), acting on the dimer dipoles. This is introduced as \( \sum \mathcal{H}_i \mathcal{S}_i \mathcal{S}_i \), in addition to the Hamiltonian defined in equation (1). Possible origins of this term in the BEDT-TTF compounds are attributed to the random

Figure 2. ME effects in a two dimensional molecular dimer system. (a) Finite \( T \) phase diagram. Spin and charge configuration in the multiferroic AFE + AFM phase is also shown. Filled purple circles, shaded ovals, and thin red and blue arrows represent molecules, charge distributions, and spins, respectively. The two kinds of dimers are labeled by A and B. (b) Calculated \( T \) dependences of the ME coefficients \( \alpha \). Red and green lines represent the results in the case where the electric field is applied along the \( x \) and \( y \) axes, respectively. (c) Calculated \( T \) dependences of the staggered magnetization \( M_{AF} \) (red line) and staggered electric polarization \( P_{AF} \) (green line). (d) Calculated \( T \) dependences of the composite spin-charge order parameter \( \tau \) (blue line) and a product of \( M_{AF} \) and the magnetic susceptibility \( \chi_s \) (orange line). (e) Net magnetization versus electric field for several \( T \). (f) A spin and charge configuration below \( T_N \) under the electric field along the \( x \) axis.
configurations of the ethylene groups in the BEDT-TTF molecules 38,39 and the random orientations of the CN groups in the anion layer 40. Artificial X-ray irradiation may also produce random potentials in samples 41,42. Relaxor-like behaviors in the dielectric constant, which might be due to random dipole configurations, are often observed experimentally in the dimer-type organic molecular solids21–23,43. The model Hamiltonian with the random electric field is analyzed by the cluster mean-field approximation, in which physical quantities are averaged with respect to the random configurations of $h_i$, and amplitude of the random field is denoted by $h$. Details are given in SI.

As shown Fig. 4a, finite values of the ME coefficients emerge below certain temperatures. In the case of the strong randomness, instead of the multiferroic AFE $+$ AFM state, the spin glass (SG) state associated with the electric-dipole glass, i.e. the charge glass (CG) state emerges. In Fig. 4b, we plot the temperature dependences of the SG order parameter ($q_S$) and the CG order parameter ($q_Q$). While the CG order parameter is always finite, the SG state sets in at a certain temperature denoted by $T_{SG}$. Any types of order parameters for the conventional magnetic and electric-dipole long-range orders are zero in a whole temperature range, unlike the case without the randomness. There is a hidden order below $T_{SG}$, i.e., the ferroic order of the spin-charge composite operator appears, as shown in Fig. 4b. It is shown in Fig. 4a that the linear ME coefficients for several amplitudes of the randomness appear in concert with $\tau$. The present ME effect is active even without the conventional magnetic and electric-dipole orders, but under the ferroic order of the spin-charge composite object. It is noted that the ME coefficient is finite, when the electric field is applied along the $y$ axis in contrast to that in the multiferroic AFE $+$ AFM phase. This is because $\sum_i (p^y S_i) / \tau$ is finite reflecting the crystal lattice symmetry.

**Discussion**

The present scenario for the ME effect has significant potentialities for actual dimer-type organic molecular solids. A possible candidate is $\kappa$-(BEDT-TTF)$_2$Cu[N(CN)$_2$]Cl. A long-range order of the dimer dipoles associated with the AFM order, which is similar to the configuration shown in Fig. 2a, was reported below the Néel temperature at approximately 27 K22, although there is a debate for a realization of the dimer dipoles 24,25. Another candidate is $\beta'$-(BEDT-TTF)$_2$ICl$_2$, where a change in the dielectric responses was observed at the Néel temperature23. The present scenario of the ME effect is also applicable to a series of TMTTF$_2$X; in the case of $X = $ SbF$_6$, a ferroelectric-type dipole order associated with the AFM order emerges44–46. The expected maximum values of the ME and inverse ME coefficients from the present theory are of the order on $10^{-6}$–$10^{-4}$ in the cgs Gauss system, in which $10^{-4}$ is the same order of the ME coefficients in Cr$_2$O$_3$47. In the multiferroic AFE $+$ AFM ordered phase the present scenario for the ME effect has significant potentialities for actual dimer-type organic molecular solids. A possible candidate is $\kappa$-(BEDT-TTF)$_2$Cu[N(CN)$_2$]Cl. A long-range order of the dimer dipoles associated with the AFM order, which is similar to the configuration shown in Fig. 2a, was reported below the Néel temperature at approximately 27 K22, although there is a debate for a realization of the dimer dipoles 24,25. Another candidate is $\beta'$-(BEDT-TTF)$_2$ICl$_2$, where a change in the dielectric responses was observed at the Néel temperature23. The present scenario of the ME effect is also applicable to a series of TMTTF$_2$X; in the case of $X = $ SbF$_6$, a ferroelectric-type dipole order associated with the AFM order emerges44–46. The expected maximum values of the ME and inverse ME coefficients from the present theory are of the order on $10^{-6}$–$10^{-4}$ in the cgs Gauss system, in which $10^{-4}$ is the same order of the ME coefficients in Cr$_2$O$_3$47. In the multiferroic AFE $+$ AFM ordered phase.

**Figure 3.** Spin and charge distributions for the spin-charge composite moment. Filled circles, shaded ovals, and thin arrows represent molecules, charge distributions, and spins, respectively. Shaded orange and green circles represent positive and negative charge distributions, respectively. The spin distribution in a dimer unit in the ferroic spin-charge composite ordered state is decomposed into a magnetic dipole moment, a magnetic quadrupole moment, and a toroidal moment.

**Figure 4.** ME effects in a two dimensional molecular dimer system in the presence of local random electric fields. (a) Calculated $T$ dependences of the ME coefficient for the several amplitudes of the random field $h$. The electric field is applied along to the $y$ direction. (b) Calculated $T$ dependences of order parameters at the random field amplitude $h = 2.5$. Order parameters for SG ($q_S$) and CG ($q_Q$) are denoted by red and green lines, respectively. A blue line represents the ferroic spin-charge composite order parameter.
in the \( \kappa \)-(BEDT-TTF) type crystal lattice, there are four kinds of domains. One is given in the spin and charge configuration shown in Fig. 2a, and other three are obtained from this configuration by flipping all the spin directions and/or the dimer-dipole directions. A tensor component of the ME response coefficient \( \kappa_{x,y} \) is only finite in the four domains, but its sign depends on a type of the domain. Thus, we expect in a multi-domain sample that observed sign and amplitude of the ME coefficient depend on a relative volume of the charge and spin domains. The ME effect proposed here has a chance to be generalized into the ME effect in the high frequency region, which will be confirmed directly by the optical measurements. The present novel ME effect in the dimer-type organic molecular solids may not only provide the new guiding principle of multiferroic materials, but also promote material designs of organic molecular solids as flexible and lightweight multifunctional materials.

**Method**

Phase diagram at finite temperature is calculated by applying the mean-field approximation to the Hamiltonian in equation (1), where \( \langle S^x \rangle, \langle Q^x \rangle, \) and \( \langle S^x Q^y \rangle \) as the order parameters are determined self-consistently. The model Hamiltonian with the random field is analyzed by the cluster mean-field approximation; spin and pseudo-motive material designs of organic molecular solids as flexible and lightweight multifunctional materials.

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Author Contributions
M.N. carried out the calculations. M.N. and S.I. analyzed the results. M.N. and S.I. wrote the paper. S.I. led the project.

Additional Information
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