Results on $\beta\beta$ decay with emission of two neutrinos or Majorons in $^{76}$Ge from GERDA Phase I

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Abstract A search for neutrinoless $\beta\beta$ decay processes accompanied with Majoron emission has been performed using data collected during Phase I of the GERmanium Detector Array (GERDA) experiment at the Laboratori Nazionali del Gran Sasso of INFN (Italy). Processes with spectral indices $n = 1, 2, 3, 7$ were searched for. No signals were found and lower limits of the order of $10^{23}$ yr on their half-lives were derived, yielding substantially improved results compared to previous experiments with $^{76}$Ge. A new result for the half-life of the neutrino-accompanied $\beta\beta$ decay of $^{76}$Ge with significantly reduced uncertainties is also given, resulting in $T_{1/2}^{\nu\nu} = (1.926 \pm 0.095) \times 10^{21}$ yr.

Keywords double beta decay · Majoron emission · enriched $^{76}$Ge

PACS 23.40.-s $\beta$ decay; double $\beta$ decay; electron and muon capture · $14.80.Va$ majorons · $21.10.Tg$ Lifetimes, widths · $27.50.+e$ mass $59 \leq A \leq 89$

1 Introduction

Neutrinoless double beta ($0\nu\beta\beta$) decay is regarded as the gold-plated process for probing the fundamental character of neutrinos. Observation of this process would imply total lepton number violation by two units and that neutrinos have a Majorana mass component. Although the main focus of experimental efforts lies on the detection of $0\nu\beta\beta$ decay mediated by light Majorana neutrino exchange, there are also many other proposed mechanisms which are being searched for. Some exotic models predict $0\nu\beta\beta$ decays proceeding through the emission of a massless Goldstone boson, called Majoron. Predictions of different models depend on its transformation properties under weak isospin, singlet [1], doublet [2] and triplet [3]. Precise measurements of the invisible width of the Z boson at LEP [4] greatly disfavour triplet and pure doublet models. Several new Majoron models have been developed subsequently in which the Majoron carries leptonic charge and cannot be a Goldstone boson [5, 6] or in which the $0\nu\beta\beta$ decay proceeds through the emission of two Majorons [7].

All these models predict different shapes of the two emitted electrons’ summed energy spectrum. The predicted spectral shapes are essentially defined by the phase space of the emitted particles:

$$\frac{dN}{dK} \sim G \sim (Q_{\beta\beta} - K)^n$$  \hspace{1cm} (1)

where $K$ is the summed energy of the two electrons, $G$ is the phase space, $Q_{\beta\beta}$ is the $Q$ value of the $0\nu\beta\beta$ decay and $n$ is the spectral index of the model. Single Majoron emitting $\beta\beta$ decays can be roughly divided into three classes, $n = 1, 2, 3$. Double Majoron emitting decays can have either $n = 3$ or $n = 7$. Their characteristic spectral shapes differ from that of two-neutrino $\beta\beta$ decay $(2\nu\beta\beta)$, for which $n = 5$. This allows for discrimination between the processes.

Experimental searches for $\beta\beta$ decay mediated by emission of one or two Majorons ($0\nu\beta\beta\chi$) have been performed by the Heidelberg-Moscow experiment (HDM) for $^{76}$Ge [8, 9]; by NEMO-2 and NEMO-3 for $^{100}$Mo, $^{116}$Cd, $^{82}$Se, $^{96}$Zr, $^{130}$Te [10, 11]; by ELEGANT V for $^{100}$Mo [12]; by DAMA [13] and by KAMLAND-Zen for $^{136}$Xe [14]. None of these experiments have seen an excess of events that could be interpreted as a Majoron signal; they reported lower limits on the half-lives of the processes that involve Majoron emission.

The $2\nu\beta\beta$ decay process conserves lepton number and is independent of the nature of the neutrino. It has been detected for eleven nuclides so far, with measured half-lives ($T_{1/2}^{\beta\beta}$) in the range of $7 \times 10^{18} - 2 \times 10^{24}$ yr [15, 16, 17]. The knowledge of $T_{1/2}^{\beta\beta}$ allows for extraction of the nuclear matrix element, $M^{2\nu}$, which can provide some constraints on that of $0\nu\beta\beta$ decay, $M^{0\nu}$, if the evaluations of $M$ for the two processes are performed within the same model [18, 19].

This paper reports on the search for neutrinoless double beta decay of $^{76}$Ge with Majoron emission ($0\nu\beta\beta\chi$) and a new analysis of the half-life of the $2\nu\beta\beta$ decay of $^{76}$Ge using data collected by the GERDA experiment during its Phase I. $2\nu\beta\beta$ decay is a well established and previously observed process, while $0\nu\beta\beta\chi$ decay is a hypothetical one. In the first case the half-life is extracted, while for the second one a limit is set. This leads to slightly different approaches in the analyses leading to different data sets and background components being used.

2 The GERDA experiment

The main aim of the GERDA experiment [20] at the Laboratori Nazionali del Gran Sasso (LNGS) of INFN in Italy is to search for $0\nu\beta\beta$ decay of $^{76}$Ge. The core of the setup is an array of high-purity germanium (HPGe) detectors made from isotopically modified material with $^{76}$Ge enriched to $\sim 86\%$ (enriched Ge), mounted in low-mass copper supports (holders) and immersed in a 64 m$^3$ cryostat filled with liquid argon (LAr). The LAr serves as cooling medium and shield against external backgrounds. The shielding is complemented by water in a...
tank of 10 m in diameter which is instrumented with photomultipliers to detect Cherenkov light generated in muon-induced showers [20].

The array of HPGe detectors is arranged in strings. Each string is enclosed with a cylinder, made from 60 µm thick Cu foil, called mini-shroud, to mitigate the background coming from the decay of 42Ar present in the LAr. Moreover, in order to prevent contamination from radon within the cryostat, a cylinder, made from 30 µm thick Cu foil, called radon-shroud, separates the central part of the cryostat, where the detectors are located, from the rest. The HPGe detector signals are read out with custom-made charge sensitive preamplifiers optimized for low radioactivity, which are operated close to the detectors in the LAr. The analog signals are digitized with 100 MHz Flash ADCs (FADC) and analyzed offline. If one of the detectors has an energy deposition above the trigger threshold (40-100 keV), all channels are read out. Reprocessed p-type coaxial detectors from the HoM [21] and IGEX [22] experiments were operated together with Broad Energy Germanium (BEGe) type detectors manufactured by Canberra [23,24].

As explained in section 5, some background components have different effects on the two detector types due to their peculiar geometry. A schematic drawing of a coaxial detector type is shown in the top part of Fig. 1, while the lower part depicts that for a BEGe type detector.

![Schematic sketch of a coaxial HPGe detector (top) and a BEGe detector (bottom) with their different surfaces and dead layers (drawings not to scale), adapted from Ref. [25].](image)

Fig. 1  Schematic sketch of a coaxial HPGe detector (top) and a BEGe detector (bottom) with their different surfaces and dead layers (drawings not to scale), adapted from Ref. [25].

### 3 Data taking and data selection

Phase I data taking lasted from November 9, 2011, to May 21, 2013. The total exposure collected comprises 19.2 kg·yr for the coaxial detectors and 2.4 kg·yr for the BEGe detectors. In this paper, the entire exposure collected by the BEGe detectors (BEGe data set) and 17.9 kg·yr from the coaxial detectors (golden data set) are used [25,26]. For the coaxial detectors, a data set collected for 1.3 kg·yr exposure during a restricted time period around the deployment of the BEGe detectors is discarded due to a higher background level. Also one of the coaxial detectors, RG2, is not considered for the data analysis starting from March 2013, as its high voltage had to be reduced below depletion voltage due to increased leakage current. The energy calibration of the detectors was performed using the information from dedicated calibration runs. For these calibration runs, three 228Th sources were lowered to the vicinity of the detectors. The stability of the energy scale was monitored by performing such calibration runs every one or two weeks. Moreover, the stability of the system was continuously monitored by injecting charge pulses into the test input of the preamplifiers. Using physics data, the interpolated FWHM values at $Q_{33}$ averaged with the exposure are $(4.8 \pm 0.2)$ keV for the coaxial detectors and $(3.2 \pm 0.2)$ keV for the BEGe detectors.

All steps of the offline processing of the GERDA data were performed within the software framework GElatio [27]. The energy deposited in each detector was extracted from the respective charge pulse by applying a approximate Gaussian filter [28]. Non-physical events, such as discharges, cross-talk and pick-up noise events, were rejected by quality cuts based on the time position of the rising edge, the information from the Gaussian filter, the rise time and the charge pulse height, which must not exceed the dynamic range of the FADCs. Pile-up and accidental coincidences were removed from the data set using cuts based on the baseline slope, the number of triggers and the position of the rising edge. The rate of pile-up and accidental coincidence events is negligible in the GERDA data due to the extremely low event rate. The loss due to mis-classification by the quality cuts was $<0.1\%$ for events with energies above 1 MeV. All events that come within 8 µs of a signal from the muon veto were rejected. Finally, only events that survive the detector anti-coincidence cut were considered. This means, that all events with an energy deposition $>50$ keV in more than one detector in the array were not taken into account. Since $2\nu\beta\beta$ and $0\nu\beta\beta$ events release their energy within a small volume inside the detectors, almost no signal events were lost by this
cut, while a part of the $\gamma$-induced background events were rejected.

4 Analysis Strategy

The two analyses described in this paper are different in the sense that for $2\nu\beta\beta$ decay a parameter is extracted for a well established and known process, while in the case of the search for $0\nu\beta\beta\chi$ decay limits for a hypothetical process are set. In order to minimize the systematic uncertainties for the extraction of the $T_{1/2}^{2\nu}$, it is favorable to use a well defined and controlled subset of the data and to use only well identified background processes. For $0\nu\beta\beta\chi$ limit setting it is favorable to maximize the exposure and to take into account all known possible background processes that can not be unambiguously detected but could mimic $0\nu\beta\beta\chi$ decay.

For the $T_{1/2}^{2\nu}$ analysis the golden data set (17.9 kg yr) with the coaxial detectors is used in order to have a large data sample obtained in well controlled experimental conditions. The Majoron analysis uses both the golden data set and the BEGe data set for a total exposure of 20.3 kg yr in order to maximize the sensitivity.

The background model for the $T_{1/2}^{2\nu}$ analysis uses a minimal number of components, assuming all sources near to the detectors [25, 29]. For the Majoron analysis, an expanded model is used [30], taking into account also additional medium and far distant positions for some of the sources. This becomes necessary when searching for rare processes such as Majoron emission, where all possible sources of background which could simulate the exotic process have to be considered. Therefore, even the slight differences resulting, for example from a variation of the source position, have to be evaluated.

In both analyses, the experimental spectra of the coaxial and BEGe detectors are analyzed using the Bayesian Analysis Toolkit (BAT) [31].

5 The background model

The background sources considered in the models were identified by their prominent structures in the energy spectra and were also expected on the basis of material screening measurements. The spectral shapes of individual background contributions were obtained by using a detailed implementation of the experimental setup in the Monte Carlo (MC) simulation framework MAGe [32]. A Bayesian spectral fit of the measured energy spectrum with the simulated spectra was performed in an energy range from 570 keV up to the end of the dynamic range at 7500 keV. The low energy limit is motivated by the $\beta$-decay of $^{39}$Ar, which gives a large contribution up to its $Q_\beta$-value of 565 keV.

The following background components were used for the extraction of the $T_{1/2}^{2\nu}$ (minimum model in Refs. [25, 29]): (1) $^{76}$Ge $2\nu\beta\beta$ decay, (2) $^{214}$Bi, $^{228}$Ac, $^{228}$Th, $^{60}$Co and $^{42}$K decays in the close vicinity of the detectors (<2 cm, represented by decays in the detector holders in the MC simulation), (3) decays of $^{60}$Co inside the detectors, constrained by the maximum expected activity from their cosmogenic activation history, (4) $^{42}$K decays in LAr assuming a uniform distribution, (5) $\alpha$-model that accounts for $\alpha$ decays originating from $^{210}$Po and $^{226}$Ra contaminations on the $p^+$ surface of the detectors as well as from $^{222}$Rn in the LAr, and finally (6) $^{214}$Bi decays on the $p^+$ surface, constrained by the estimated $^{226}$Ra activity from the $\alpha$-model.

The parameters of all components besides the constrained ones were given a flat prior probability distribution. There are no strong correlations between the model parameters since all considered background components have characteristic features such as $\gamma$-ray lines or peak-like structures at different energies. The ratios of the $\gamma$-ray line intensities from the individual considered background sources suggest contaminations dominantly in locations close to the detectors. Hence, the minimum model takes into account only the close-by source locations. Nevertheless, the screening measurements indicate contaminations of materials in farther locations as well. An additional contribution can come from $^{42}$K decays at or near the detector $n^+$ surfaces (see Fig. 1) with a specific activity higher than that for the uniform distribution assumption. This component is the dominating one for the BEGe data set, as the thinner dead layer thickness of BEGes of roughly 1 mm allows penetration of the electrons emitted in the decay of $^{42}$K to the active volume, while for coaxial detectors the dead layer thickness of $\sim 2$ mm efficiently shields this background component.

The spectral shapes of the contributions from the background sources without significant multiple $\gamma$ peaks at different source locations differ only marginally. This makes it impossible to pinpoint the exact source locations given the available statistics of the measured spectra. Therefore, variations of the source locations for the considered decays were taken into account when evaluating the systematic uncertainty on $T_{1/2}^{2\nu}$. For the Majoron analysis additional background components were used [30], including also medium and far distant contributions. For the coaxial detectors $^{42}$K on the $n^+$ and on the $p^+$ contacts was added to the list of the close sources of the previous background model. For medium distances, i.e. between 2 cm and 50 cm from the detectors, contributions from the following sources
were added: $^{214}$Bi, $^{228}$Th and $^{228}$Ac. A $^{228}$Th contamination was chosen as a representative for far distant sources (above 50 cm). Whenever possible, screening measurements were used to constrain the lower limit of the expected background events.

In the Majoron analysis, also the data collected with the BEGe diodes were used in order to maximize the exposure. Consequently, the background model developed for these detectors was used [25,30]. The same close, medium and far distant sources as for the coaxial detectors were used. $^{68}$Ge was added as internal source. This was necessary in order to take into account the cosmic activation of the germanium due to the recent production of these diodes.

6 Determination of the half-life of $2\nu\beta\beta$ decay

6.1 Analysis

The $T_{1/2}^{2\nu}$ of $2\nu\beta\beta$ decay of $^{76}$Ge was determined considering the golden data set of Phase I, amounting to an exposure of 17.9 kg-yr, and using the background model prediction for the contribution of the $2\nu\beta\beta$ spectrum to the overall energy spectrum. Details of the background analysis can be found in Ref. [29].

The global fit for the background modeling was performed on the summed energy spectrum of the coaxial detectors using a bin width of 30 keV. Thus, the scaling parameter of the $2\nu\beta\beta$ spectrum in the model, $N_{AV}^{\text{fit}}$, gives the number of events in the $2\nu\beta\beta$ spectrum in the fit window of 570–7500 keV for all detectors. Using this result for the number of measured $2\nu\beta\beta$ events, the half-life is calculated as

$$T_{1/2}^{2\nu} = \left(\frac{\ln 2}{N_{AV}^{\text{fit}}} \sum_{i=1}^{N_{\text{det}}} M_i t_i f_{76,i} \left[f_{AV,i} \varepsilon_{AV,i}^{\text{fit}} + (1 - f_{AV,i}) \varepsilon_{DL,i}^{\text{fit}} \right] \right),$$

where $N_A$ is Avogadro’s constant and $m_{\text{enr}} = 75.6$ g is the molar mass of the enriched material. The summation runs over all the detectors ($N_{\text{det}}$) considered in the data set. All detector related parameters like the detector mass ($M_i$), the time of the data taking for each detector ($t_i$), the fraction of $^{76}$Ge atoms ($f_{76,i}$), the active volume fraction ($f_{AV,i}$), and the detection efficiencies in the active volume ($\varepsilon_{AV,i}^{\text{fit}}$) and in the dead layer ($\varepsilon_{DL,i}^{\text{fit}}$) are taken into account separately for the individual detectors. All values are listed in Table 1. The efficiency $\varepsilon_{AV,i}^{\text{fit}}$ ($\varepsilon_{DL,i}^{\text{fit}}$) corresponds to the probability that a $2\nu\beta\beta$ decay taking place in the active volume (dead layer) of the detector deposits detectable energy in the fit window considered for the background model.

### Table 1

Parameters for the coaxial detectors (upper part) and for the BEGe detectors (lower part): live time, $t$, total mass, $M$, the fraction of $^{76}$Ge atoms, $f_{76}$, and the active volume fraction, $f_{AV}$. For the coaxial detectors, the first uncertainty on $f_{\text{act}}$ is the uncorrelated part, the second one the correlated contribution. The values for $M$, $f_{76}$ and $f_{AV}$ are taken from Ref. [25].

| detectors          | $t$ [days] | $M$ [kg] | $f_{76}$ [%] | $f_{AV}$ [%] |
|--------------------|------------|----------|--------------|--------------|
| enriched coaxial detectors |            |          |              |              |
| GD32B              | 280.0      | 0.717    | 87.7 ± 1.3   | 89.0 ± 2.7   |
| GD32C              | 304.6      | 0.743    | 87.7 ± 1.3   | 91.1 ± 3.0   |
| GD32D              | 282.7      | 0.723    | 87.7 ± 1.3   | 92.3 ± 2.6   |
| GD35B              | 301.2      | 0.812    | 87.7 ± 1.3   | 91.4 ± 2.9   |
| enriched BEGe detectors |        |          |              |              |

The detection efficiencies, on average $\varepsilon_{AV,I}^{\text{fit}} = 0.667$ and $\varepsilon_{DL}^{\text{fit}} = 0.011$, are obtained through dedicated MC simulations. The statistical uncertainty due to the number of simulated events is on the order of 0.1 %.

The background model resulted in a scaling parameter of $N_{AV}^{\text{fit}} = 25690 \pm 310$ for the $2\nu\beta\beta$ spectrum, which is the best fit parameter. The uncertainty is given by the smallest 68% probability interval of the marginalized posterior probability distribution. Using this result, the half-life derived according to Eq. 2 is

$$T_{1/2}^{2\nu} = 1.926^{+0.022}_{-0.022} \times 10^{21} \text{ yr}.$$  

6.2 Systematic Uncertainties

The systematic uncertainties affecting the results for $T_{1/2}^{2\nu}$ were grouped into the three categories (i) detector parameters and fit model, (ii) MC simulation, and (iii) data acquisition and selection. The contributions to the total systematic uncertainty on $T_{1/2}^{2\nu}$ are summarized in Table 2.

(i) detector parameters and fit model

- The systematic uncertainty on the active $^{76}$Ge exposure ($\mathcal{E}_{AV,76}$) was determined using a MC approach. $\mathcal{E}_{AV,76}$ is defined as

$$\mathcal{E}_{AV,76} = \sum_{i=1}^{N_{\text{det}}} M_i t_i f_{AV,i} f_{76,i}.$$  

For evaluating its uncertainty, the parameters of the individual detectors were randomly sampled from
Table 2 Contributions to the systematic uncertainty on $T_{1/2}^{2\nu}$ taken into account in this work. The total systematic uncertainty is obtained by combining the individual contributions in quadrature.

| Item                          | Uncertainty on $T_{1/2}^{2\nu}$ [$\%$] |
|-------------------------------|----------------------------------------|
| Active $^{76}$Ge exposure     | $\pm 4$                                 |
| Background model components   | $\pm 1.4$                               |
| Binning                      | $\pm 0.5$                               |
| Shape of the $2\nu\beta\beta$ spectrum | $< 0.1$                               |
| Subtotal fit model            | $\pm 4.3$                               |
| Precision of the Monte Carlo geometry model | $\pm 1$                                 |
| Accuracy of the Monte Carlo tracking | $\pm 2$                                 |
| Subtotal Monte Carlo simulation | $\pm 2.2$                              |
| Data acquisition and handling | $< 0.1$                                |
| Total                         | $\pm 4.8$                               |

Gaussian distributions with mean values and standard deviations according to the corresponding values listed in Table 1. The correlated terms for $f_{AV}$ were also taken into account. The uncertainty on the live time $t$ is 0.3 %, whereas the total detector masses are known with good accuracy (uncertainty smaller than 0.1 %). The calculation yields $E_{AV,76} = (13.45 \pm 0.54)$ kg yr. The uncertainty of 4% is driven by the uncertainties on $f_{AV}$ and $f_{76}$, which mainly affect the number of $^{76}$Ge nuclei in the active volume of the detectors, with a relatively smaller impact on the detection efficiency for the background sources.

The reference background model used for determining $T_{1/2}^{2\nu}$ accounts only for the dominant source locations in the setup. The systematic uncertainty due to the choice of the background model components was evaluated by repeating the global fit with alternative models, which account for different source locations for all the background sources considered in the reference model. The model that accounts for $^{228}$Th and $^{228}$Ac contributions also in the radon-shroud instead of only in the holders results in a 1.4 % longer $T_{1/2}^{2\nu}$. The same increase occurs if $^{40}$K in the radon-shroud is added to the model components. The model including the contribution from $^{214}$Bi in the radon-shroud in addition to the $p^+$ surface and holders yields a 0.7 % longer $T_{1/2}^{2\nu}$. In all the cases mentioned above, the contribution from background in the $2\nu\beta\beta$ spectrum region increases, since the peak-to-Compton ratio of the $\gamma$-rays decreases for farther source locations leading to longer $T_{1/2}^{2\nu}$ estimates. Excluding contributions from very close source locations, like $^{214}$Bi on the $p^+$ surface and $^{60}$Co on the germanium, results in a smaller increase of the best $T_{1/2}^{2\nu}$ estimate. In this case, the contributions from these components are compensated by $^{214}$Bi and $^{60}$Co decays in the holders, respectively. Consequently, the source locations are moved further out with respect to the reference model. Consistently, the models that include additional contributions from close source locations yield a decrease in the $T_{1/2}^{2\nu}$ value, e.g. including $^{214}$Bi in LAr close to the $p^+$ surface (-1.0 %) or $^{42}$K on the $n^+$ (-1.2 %) and $p^+$ (-0.6 %) surfaces. Comparing alternative background models to the reference one, the deviations in the $T_{1/2}^{2\nu}$ result range between -1.2 % and +1.4 %.

- For the standard fit, a bin width of 30 keV was used for the data and MC energy spectra. In order to take into account the systematic uncertainty related to binning effects, the fit was repeated twice using bin widths of 10 and 50 keV. The bin width of 10 keV was chosen in order to minimize as much as possible the bin size taking into account the energy resolution of $\approx 4.5$ keV of the coaxial detectors and the necessity to have enough statistics in all bins. Above 50 keV, peak structures are washed out, leading to a deterioration of the fit. The deviations in the $T_{1/2}^{2\nu}$ result range between -0.5 % and +0.5 % with respect to that using the standard bin width.

- The primary spectrum of the two electrons emitted in the $2\nu\beta\beta$ decay of $^{76}$Ge, which was then fed into the MC simulation, was sampled according to the distribution given in Ref. [33] implemented in DECAYO [34]. The systematic uncertainty due to the assumed $2\nu\beta\beta$ spectral shape was evaluated by comparing the spectrum generated by DECAYO to the one given in Ref. [35]. Considering the analysis window used for background modeling, the maximum deviation is 0.2 % and the total deviation of the integral in the analysis window is 0.1 %. When the fit with the background model is repeated using the
comes from the uncertainty on the active 

The largest contribution to the systematic uncertainties 

of 4.9 % is dominated by the systematic uncertainties. 

The total uncertainty 

with the latter combining in quadrature the statistical 

implemented in 

MaGe 

from the precision of the experimental geometry model 

(ii) MC simulation 

The uncertainty related to the MC simulation arises 

from the precision of the experimental geometry model 

implemented in MAGE (1 %) and from the accuracy of 

particle tracking (2 %) performed by GEANT4 [38,39]. 

The total MC simulation uncertainty was estimated to 

be 2.2 % by summing in quadrature the aforementioned 

contributions.

(iii) Data acquisition and selection 

The trigger and reconstruction efficiencies for physical 

events are practically 100 % above 100 keV in GERDA. 

The performance of the quality cuts applied in Phase I 

data has been investigated through a visual analysis. 

The total uncertainty related to data acquisition 

and selection was estimated to be less than 0.1 %.

Summing in quadrature the uncertainties of the three 

groups gives a total systematic uncertainty of ±4.8 %.

6.3 Results and Discussion

Fig. 2 shows the experimental data together with the 

best fit model for the golden data set. The different 

components of the minimum background model are also 

reported. The model is able to reproduce the experi- 

mental data well, as shown in the lower panel of the 

figure by the residuals.

The best estimate of the $T_{1/2}$ of the $2\nu\beta\beta$ decay of 

76Ge is:

$$T_{1/2}^{2\nu} = \left( 1.926^{+0.025}_{-0.022,\text{stat}} ^{+0.092}_{-0.092,\text{syst}} \right) \cdot 10^{21} \text{ yr}$$

$$= (1.926 \pm 0.095) \cdot 10^{21} \text{ yr}, \quad (5)$$

with the latter combining in quadrature the statistical 

(fit) and systematic uncertainties. The total uncertainty 

of 4.9 % is dominated by the systematic uncertainties.

The largest contribution to the systematic uncertainties 

comes from the uncertainty on the active 76Ge exposure 

(4 %), which can only be reduced by performing new 

and more precise measurements of the active masses 

of the coaxial detectors. Other significant contributions 

are related to the Monte Carlo simulations (2.2 %) and 
to the background model assumptions ($^{+1.4}_{-1.2}$ %). The latter 
have been significantly reduced in this analysis compared 
to the analysis of the first 5 kg yr of Phase I data 
reported in Ref. [41], where the systematic uncertainty 
due to the background model was $-2.1$ %. The new result 
is in good agreement with that mentioned above. 
Adding further identified components to the reference 
background model results in a slight increase of the best 
$T_{1/2}^{2\nu}$ estimate.

The background level achieved in GERDA Phase I 
is about one order of magnitude lower with respect 
to predecessor 76Ge experiments, and has allowed the 
measurement of $T_{1/2}^{2\nu}$ with an unprecedented signal-to- 
background ratio of 3:1 in the 570–2039 keV interval.

The ratio amounts to 4:1 for the smaller interval of 
600–1800 keV.

7 Limits on Majoron-emitting double $\beta$-decays of 76Ge

7.1 Analysis

The search for $0\nu\beta\beta_{\chi}$ was performed using the golden 
and BEGe data sets, amounting to a total exposure of 
20.3 kg yr. The analysis employed the background 
model described in section 5. The information from the 
two data sets was combined in one fit, while keeping 
their energy spectra distinct. A separate fit was per- 
formed for each spectral index, containing the back- 
ground contributions, the contributions from $2\nu\beta\beta$ de- 
cay, and also the Majoron component under study. A 
single parameter, $T_{1/2}^{2\nu}$, is considered common for the 
two data sets. It is defined as the half-life of the respec- 
tive Majoron accompanied mode.

In order to improve the detection efficiency for the 
Majoron processes with low $n$ ($n = 1, 2$), a slightly 
different event selection was used with respect to the 
$T_{1/2}^{2\nu}$ analysis. If an event occurs with energy deposition 
in two detectors and the energy deposit in the detector 
where the decay took place is below the threshold for the anti-coincidence cut, the event contributes to the 
energy spectrum of the other detector. Therefore, 
when determining the total energy spectrum resulting 
from decays in one of the detectors, the energy spectra 
from all detectors in the array have to be taken into 
account. Such a selection has no impact on the detection 
efficiency for the Majoron process with $n = 3$ and 
7 and $2\nu\beta\beta$ decay. The content of the $i$-th bin in the 
combined energy spectrum of all $N_{\text{det}}$ detectors in the
array, for decays taking place in the active and dead part of detector $\alpha$, becomes:

$$
\lambda_i^{0,0\nu\chi} = \frac{(\ln 2) N_A}{m_{\nu_\alpha} T_{1/2,\alpha}^0} M_\alpha f_{0,\alpha} \cdot \left[ f_{AV,\alpha} \sum_{j=1}^{N_{det}} t_j \epsilon_{AV,j}^{0,0\nu\chi} \Phi_{AV,i,j}^{0,0\nu\chi} \right] + (1 - f_{AV,\alpha}) \sum_{j=1}^{N_{det}} t_j \epsilon_{DL,j}^{0,0\nu\chi} \Phi_{DL,i,j}^{0,0\nu\chi} 
$$

(6)

with $\Phi_{AV,i,j}^{0,0\nu\chi}$ ($\Phi_{DL,i,j}^{0,0\nu\chi}$) giving the content of the $i$-th bin of the normalized energy distribution recorded with detector $j$ for $0\nu\beta\beta\chi$ taking place in the active (dead) volume of detector $\alpha$. Summing up the simulations of decays in all $N_{det}$ detectors results in the final model spectrum:

$$
\lambda_i^{0,0\nu\chi} = \sum_{\alpha=1}^{N_{det}} \lambda_i^{0,0\nu\chi}. 
$$

(7)

For all four Majoron modes ($n = 1, 2, 3, 7$) only lower limits on the half-life can be given. They were obtained from the 90% quantiles of the marginalized posterior distributions. These lower limits for $T_{1/2}^{0,0\nu\chi}$, not taking into account the systematic uncertainties, are in units of $10^{23}$ yr: $>4.4$, $>1.9$, $>0.9$, and $>0.4$ for $n = 1, 2, 3$, and 7, respectively. The respective half-life of the $2\nu\beta\beta$ process derived from this analysis amounts to in units of $10^{21}$ yr: $1.96 \pm 0.03_{\text{stat}}$, $1.97 \pm 0.03_{\text{stat}}$, $1.98 \pm 0.03_{\text{stat}}$, and $1.99 \pm 0.03_{\text{stat}}$. Within the uncertainties coming from the different background models and the different data

---

**Fig. 2** Upper panel: experimental data (markers) and the best fit model (black histogram) for the golden data set. The contribution from $2\nu\beta\beta$ (green) and from the single background components are also shown. Lower panel: ratio between experimental data and the prediction of the best fit model. The green, yellow and red regions are the smallest intervals containing 68%, 95% and 99% probability for the ratio assuming the best fit parameters, respectively [40].
sets of the two analyses, the derived $T_{1/2}^{0\nu\beta\beta}$ values are in agreement ($<1\sigma$) with that discussed in section 6.3.

7.2 Systematic Uncertainties

The systematic uncertainties were divided into the three categories (i) detector parameters and fit model, (ii) MC simulation, and (iii) data acquisition and selection.

(i) detector parameters and fit model

Uncertainties from the fitting procedure were folded into the posterior distribution of $T_{1/2}^{0\nu\beta\beta}$ with a MC approach. Each source of uncertainty is described by a probability distribution. The fitting procedure was repeated 1000 times, each time drawing a random number for each source of uncertainty according to its probability distribution:

- Material screening measurement results were used to constrain the minimum number of events expected from close and medium distant sources of the $^{214}$Bi and $^{228}$Th decays. Gaussian distributions describing these lower limits used in the fit were derived from the mean and standard deviations of the screening measurements. For details see Ref. [25].

- As for the $T_{1/2}^{0\nu\beta\beta}$ analysis, the standard fit uses a bin width of 30 keV for the data and MC energy spectra. In order to determine the systematic uncertainty related to binning effects, the bin width was sampled uniformly from 10 keV to 50 keV.

- Uncertainties on the active volume fractions enter the model in several ways. On the one hand, the MC energy spectra for all internal sources, that is for $2\nu\beta\beta$, $0\nu\beta\beta\chi$, $^{60}$Co, and $^{68}$Ga decays, are affected, as the fraction of decays taking place in the active and dead part of the detectors changes with changing $f_{AV}$. On the other hand, the uncertainty on the active volume fraction also plays a role for the shape of the energy spectrum due to $^{42}$K decays on the $n^+$ surface. Larger $f_{AV}$ means thinner $n^+$ dead layer and thus the possibility of an increased contribution from the electrons to the spectrum. For smaller $f_{AV}$ and thicker $n^+$ dead layer, their contributions are expected to be reduced. The active volume fraction for each detector was sampled from a Gaussian distribution with mean and standard deviation according to Table 1. For the coaxial detectors, the partial correlations of the uncertainty were taken into account. The simulated spectra of the internal sources as well as of the $^{42}$K decays on the $n^+$ surface are composed according to the sampled active volume fractions.

- The uncertainty on the fraction of enrichment in $^{76}$Ge of the germanium that constitutes the detectors plays a role when converting the number of events attributed to $0\nu\beta\beta\chi$ into $T_{1/2}^{0\nu\beta\beta}$. The probability distribution of $f_{0\nu}$ for each detector is given by a Gaussian function with mean values and standard deviations as listed in Table 1.

- The data does not allow the resolution of the ambiguity regarding the exact positions of the near and medium distant sources. The $^{214}$Bi decays serve as a representative in order to estimate the impact of this uncertainty. Their near position is represented by decays in the holders, in the mini-shroud or on the $n^+$ surface of the detectors, each having a probability of 1/3 in the sampling process. The medium distant position is represented by decays in the radon-shroud or in the LAr, having a probability 1/2 in contrast.

- Extensive studies of the characteristics of the BEGe diodes suggest the presence of a transition layer between the region where the detector is fully efficient and the external dead region [36,37]. An uncertainty as high as $\pm 0.5\%$ on the lower limits of $T_{1/2}^{0\nu\beta\beta}$ is estimated for this effect in the case of the BEGe detectors. This uncertainty was folded into the total marginalized posterior distribution a posteriori. The corresponding uncertainty for the coaxial detectors is estimated to be negligible.

The marginalized posterior distributions for $T_{1/2}^{0\nu\beta\beta}$ derived from each of the 1000 individual fits were summed up. The resulting total marginalized posterior distribution accounts for the statistical as well as for the listed systematic uncertainties related to the fit model.

As for the $T_{1/2}^{0\nu\beta\beta}$ analysis, the uncertainties on the active volume fractions and on the enrichment fractions are major contributions to the total uncertainty on the limits for $T_{1/2}^{0\nu\beta\beta}$. However, the largest source of uncertainty is the composition of the fit model and the individual background contributions. In the case of $n = 1$, a fit with a bin width of 50 keV weakens the limit by $\approx 16\%$ compared to the standard fit, while the result for $T_{1/2}^{0\nu}$ is not affected at all. The stability of the $T_{1/2}^{0\nu}$ results shows the validity of the fit. The use of the alternative close and medium distant source positions for $^{214}$Bi decays leads to maximal variations of $+8.3\%$ and $-12.6\%$ of the limit on $T_{1/2}^{0\nu\beta\beta}$.

(ii) MC simulation

As in the case of the $T_{1/2}^{0\nu\beta\beta}$ measurement, a total MC simulation uncertainty of 2.2% has to be taken into account for effects related to the geometry implementation and particle tracking. It is folded into the total marginalized posterior distributions. No effect on the lower limits is observed for any of the spectral modes.

(iii) Data acquisition and selection
Table 3: Experimental results for the limits on $T_{1/2}^{0\nu\chi}$ of $^{76}\text{Ge}$ for the Majoron models given in Refs. [7,42,43,44]. The first section considers lepton number violating models (I) allowing $0\nu\beta\beta$ decay, while in the second section lepton number conserving models (II) are listed, where $0\nu\beta\beta$ decay is not allowed. The first column gives the model name, the second the spectral index, $n$, the third the information on whether one Majoron, $\chi$, or two Majorons, $\chi\chi$, is emitted, the fourth if the Majoron is a Goldstone boson, the fifth provides its lepton number, $L$, the sixth the experimental limit on $T_{1/2}^{0\nu\chi}$ of $^{76}\text{Ge}$ obtained in this analysis. The nuclear matrix elements, $\mathcal{M}^{0\nu\chi}$, the phase space factor, $G^{0\nu\chi}$, and the resulting effective couplings, $(g)$, are given in the seventh, eighth and ninth columns, respectively. The limits on $T_{1/2}^{0\nu\chi}$ of $^{76}\text{Ge}$ for the Majoron models and $(g)$ correspond to the 90% quantiles of the marginalized posterior probability distribution. For the case of $n = 1$, the nuclear matrix element, $\mathcal{M}^{0\nu\chi}$, from Refs. [45,46,47,48,49,50,51] and the phase space factor, $G^{0\nu\chi}$, from Ref. [52] are used for the calculation of $(g)$. The given range covers the variations of $\mathcal{M}^{0\nu\chi}$ in these works. For $n = 3$ and 7, $(g)$ is determined using the matrix elements and phase space factors from Ref. [42]. The results for $0\nu\beta\beta\chi$ ($n = 3, 7$) account for the uncertainty on $\mathcal{M}^{0\nu\chi}$. For $n = 2$, only the experimental upper limit is given.

| Model | $n$ | Mode | Goldstone boson | $L$ | $T_{1/2}^{0\nu\chi}$ [10$^{23}$yr] | $\mathcal{M}^{0\nu\chi}$ | $G^{0\nu\chi}$ [yr$^{-1}$] | $(g)$ |
|-------|-----|------|----------------|----|-----------------|----------------|-----------------|-----|
| IB    | 1   | $\chi$ | no             | 0  | $> 4.2$         | $(2.30 - 5.82) \times 10^{-17}$ | $< (3.4 - 8.7) \times 10^{-5}$ |
| IC    | 1   | $\chi$ | yes            | 0  | $> 4.2$         | $(2.30 - 5.82) \times 10^{-17}$ | $< (3.4 - 8.7) \times 10^{-5}$ |
| ID    | 3   | $\chi\chi$ | no          | 0  | $> 0.8$         | $10^{-3 \pm 1}$ | $6.32 - 10^{-19}$ | $< 21^{\pm 4.5}$ |
| IE    | 3   | $\chi\chi$ | yes          | 0  | $> 0.8$         | $10^{-3 \pm 1}$ | $6.32 - 10^{-19}$ | $< 21^{\pm 4.5}$ |
| IF    | 2   | $\chi$ | bulk field    | 0  | $> 1.8$         | –                  | –                  | –     |
| IB    | 1   | $\chi$ | no             | -2 | $> 4.2$         | $(2.30 - 5.82) \times 10^{-17}$ | $< (3.4 - 8.7) \times 10^{-5}$ |
| IIC   | 3   | $\chi$ | yes            | -2 | $> 0.8$         | 0.16                | $2.07 \times 10^{-19}$ | $< 4.7 \times 10^{-2}$ |
| IID   | 3   | $\chi\chi$ | no          | -1 | $> 0.8$         | $10^{-3 \pm 1}$ | $6.32 - 10^{-19}$ | $< 21^{\pm 4.5}$ |
| IIE   | 7   | $\chi\chi$ | yes          | -1 | $> 0.3$         | $10^{-3 \pm 1}$ | $1.21 \times 10^{-18}$ | $< 22^{\pm 4.9}$ |
| IIF   | 3   | $\chi$ | gauge boson   | -2 | $> 0.8$         | 0.16                | $2.07 \times 10^{-19}$ | $< 4.7 \times 10^{-2}$ |

The uncertainty from data acquisition and selection is estimated to be below 0.1% and does not alter the derived limits on $T_{1/2}^{0\nu\chi}$.

7.3 Results and Discussion

Fig. 3 shows the global model for the case of spectral index $n = 1$ together with the energy spectra for both the coaxial and the BGe data sets. The contributions from the background contaminations, from the $2\nu\beta\beta$ decay only, and the combined spectra from the background contaminations and $2\nu\beta\beta$ decay are drawn separately. The $35868$ events in the data spectrum of the golden data set were matched with $35834$ events in the best-fit model for $n = 1$. Of those events, in the best fit, $54.5$ are attributed to $0\nu\beta\beta\chi$. For the BGe data set, the best-fit model contains $5081.4$ counts for the $5035$ measured events. In this fit, $7.8$ events are attributed to $0\nu\beta\beta\chi$ decay. The limit of $T_{1/2}^{0\nu\chi}$ at $90\%$ C.I. derived from the fit is also drawn (green histogram). The upper limits at $90\%$ C.I. for the remaining three modes are reported for illustrative purpose (blue histogram for $n = 2$, orange for $n = 3$ and red for $n = 7$). The maximum of the corresponding distributions shifts to higher energy with the diminishing of the spectral index $n$. The resulting lower limits on $T_{1/2}^{0\nu\chi}$, determined as the $90\%$ quantiles of the posterior probability distributions and taking into account all uncertainties related to the fit model, are (in units of $10^{23}$ yr): $>4.2$, $>1.8$, $>0.8$ and $>0.3$ for $n = 1, 2, 3$ and $7$, respectively. The results are summarized in Table 3 for the different Majoron models.

The limits on $T_{1/2}^{0\nu\chi}$ presented here are the most stringent limits obtained to date for $^{76}\text{Ge}$. The limits for $n = 1$ and $n = 3$ are improved by more than a factor six [9], the limit for $n = 7$ is improved by a factor five [8] compared to previous measurements. The limit for the mode with $n = 2$ is reported here for the first time.

From the lower limits on $T_{1/2}^{0\nu\chi}$, upper limits on the effective neutrino-Majoron coupling constants $(g)$ for the models with $n = 1, 3$ and $7$ can be calculated using the following equations:

$$1/T_{1/2}^{0\nu\chi} = |\langle g \rangle|^2 \cdot G^{0\nu\chi}(Q_{\beta\beta}, Z) \cdot |\mathcal{M}^{0\nu\chi}|^2$$

(8)

and

$$1/T_{1/2}^{0\nu\chi} = |\langle g \rangle|^4 \cdot G^{0\nu\chi\chi}(Q_{\beta\beta}, Z) \cdot |\mathcal{M}^{0\nu\chi\chi}|^2$$

(9)

for single and double Majoron emission, respectively. The matrix element for the models with $n = 1$ (IB, IC and IIB) are taken from Refs. [45,46,47,48,49,50,51], whereas the phase space factor is that of Ref. [52]. The matrix elements for the models with $n = 3$ (ID, IE, IIC, IID, IIF) and with $n = 7$ (IE) as well as the corresponding phase space factors are taken from Ref. [42]. The results for the upper limits on $(g)$ are also
shown in Table 3. The coupling constants allow a comparison with other isotopes. The best limits on $0\nu\beta\beta$ decay of isotopes other than $^{76}\text{Ge}$ have been obtained for $^{100}\text{Mo}$ [10] and $^{136}\text{Xe}$ [14]. When comparing with the case of $^{100}\text{Mo}$, it becomes obvious that the limits on $T_{1/2}^{0\nu\chi}$ determined in the present analysis are about one order of magnitude more stringent, for the case of $n = 7$ even two orders of magnitude. However, due to the differences in the matrix elements and the phase space factors, the resulting limits on $\langle g \rangle$ from $^{100}\text{Mo}$ and $^{76}\text{Ge}$ are comparable. The limits for $\langle g \rangle$ derived from $^{136}\text{Xe}$ are a factor of two to five more stringent due to the higher limits that had been measured for $T_{1/2}^{4\nu\chi}$.

8 Conclusions

Phase I of the GERDA experiment, located at the INFN Laboratori Nazionali del Gran Sasso (LNGS) in Italy, has been executed between November 2011 and May 2013. Utilizing the collected exposure of Phase I, an improved result of the half-life of the $2\nu\beta\beta$ process in $^{76}\text{Ge}$ was obtained and new limits for the half-lives of the Majoron-emitting double beta decays were produced.
The half-life for the $2\nu\beta\beta$ process is determined to be:

$$T_{1/2}^{2\nu} = (1.926 \pm 0.095) \cdot 10^{21} \text{ yr} .$$  \hspace{1cm} (10)

Thanks to the extremely low background level in the GERDA experiment, with a signal-to-background ratio of 3:1 in the 570–2039 keV interval and a refined background model, the measurement has an unprecedented precision ($<5\%$) with respect to previous experiments using $^{76}$Ge. The new result is in good agreement with the one derived from a smaller data set with 5 kg·yr exposure [41]. The inclusion of more components into the reference background model results in a slight increase of the best estimate for $T_{1/2}^{2\nu}$.

Majoron emission processes were searched for in the energy spectra using an exposure of 20.3 kg·yr. The analysis was performed for all four possibilities of the spectral index $n$ ($n = 1, 2, 3, \text{ and } 7$). No indication for a contribution of $0\nu\beta\beta\chi$ was found in any of the cases. Lower limits on the half-lives, $T_{1/2}^{0\nu\chi}$, were determined from the quantiles of 90\% probability of the marginalized posterior probability distributions. The results constitute the most stringent limits on $T_{1/2}^{0\nu\chi}$ of $^{76}$Ge obtained to date. For the standard mode ($n = 1$), the lower limit is determined to be:

$$T_{1/2}^{0\nu\chi} > 4.2 \cdot 10^{21} \text{ yr} .$$  \hspace{1cm} (11)

From the lower limit on $T_{1/2}^{0\nu\chi}$, an upper limit on the effective neutrino-Majoron coupling constant, $\langle g \rangle$, can be inferred:

$$\langle g \rangle < (3.4 - 8.7) \cdot 10^{-5} .$$  \hspace{1cm} (12)

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