Attentive and Contrastive Learning for Joint Depth and Motion Field Estimation

Seokju Lee  Francois Rameau  Fei Pan  In So Kweon
Korea Advanced Institute of Science and Technology (KAIST)
{seokju91,rameau.fr,feipan664}@gmail.com, iskweon77@kaist.ac.kr

Abstract

Estimating the motion of the camera together with the 3D structure of the scene from a monocular vision system is a complex task that often relies on the so-called scene rigidity assumption. When observing a dynamic environment, this assumption is violated which leads to an ambiguity between the ego-motion of the camera and the motion of the objects. To solve this problem, we present a self-supervised learning framework for 3D object motion field estimation from monocular videos. Our contributions are two-fold. First, we propose a two-stage projection pipeline to explicitly disentangle the camera ego-motion and the object motions with dynamics attention module, called DAM. Specifically, we design an integrated motion model that estimates the motion of the camera and object in the first and second warping stages, respectively, controlled by the attention module through a shared motion encoder. Second, we propose an object motion field estimation through contrastive sample consensus, called CSAC, taking advantage of weak semantic prior (bounding box from an object detector) and geometric constraints (each object respects the rigid body motion model). Experiments on KITTI, Cityscapes, and Waymo Open Dataset demonstrate the relevance of our approach and show that our method outperforms state-of-the-art algorithms for the tasks of self-supervised monocular depth estimation, object motion segmentation, monocular scene flow estimation, and visual odometry.

1. Introduction

The simultaneous estimation of the camera motion and scene geometry is a fundamental research topic in 3D computer vision. Traditionally, this problem is tackled by feature-based methods [33], or direct approaches [14] that minimizes the photometric inconsistency among warped adjacent frames. A pioneering work based on deep neural network (DNN) [44] uses the photometric error map as a self-supervisory signal to jointly train a depth and a motion network. Inspired by this baseline structure, self-supervised depth, and motion learning framework has been widely stud-

![Figure 1](image-url)

**Figure 1.** We introduce a unified motion modeling with our dynamics attention module (DAM) and a novel motion learning technique via contrastive sample consensus (CSAC). The last row shows synthesized views from the predicted depth and motion field. Compared to the baseline, our model learns the object motion fields in a more semantically plausible way, which enhances the distinction between the object and the background area. This is a video figure, best viewed in Adobe Reader.
dynamic scenes.

Recently, learning the objects’ motion together with the camera’s ego-motion and the depth has gain interest for dynamic scene understanding [6, 26, 19, 7, 8, 25, 12, 4, 23, 28]. We can distinguish mostly two types of approaches, namely the stereo-based and the monocular-based techniques. The stereo-based techniques [6, 26] take advantage of this sensor to disentangle the motion of static background and that of moving objects in the scene. For monocular systems, the ambiguity between the depth, ego-motion, and objects’ motion becomes more intricate due to the unavailability of metric depth for each frame. Therefore, Monocular-based systems [7, 25, 28] rely on instance segmentation labels to reduce this ambiguity. Despite compelling results, the need for highly expensive human-labeled data constitute an important limitation for their deployment and reduce the interest of the self-supervised depth and motion prediction framework.

To reduce the data dependency problem and to offer more versatility, we propose a novel self-supervised learning framework for depth, camera motion, and object motion field estimation using weak semantic prior (i.e., 2D object bounding boxes) as illustrated in Fig. 1. A major benefit of the proposed pipeline is that it helps to reduce the ambiguity between the camera’s ego-motion and the objects’ motion with cheaper data labels. The distinctive points of our approach are summarized as follows:

- We design a dynamics attention module that enables to train motion features dynamically when estimating the motion of a camera and objects through a two-stage projection. We highlight that motion features can be efficiently extracted by disentangling dynamic objects and static backgrounds through the simple mechanism of attention modules within the shared motion encoder.

- We propose a contrastive sample consensus for semantically plausible object motion field learning. Considering the rigid body characteristics of dynamic objects, we design a learning technique that effectively improves the capability to distinguish object’s motion boundary.

- We show that the proposed scheme achieves favorable results in motion segmentation, monocular depth and scene flow estimation, and visual odometry on the KITTI, Cityscapes, Waymo Open Dataset.

2. Related Works

2.1. Joint Training of Depth and Motion from Monocular Videos

Zhou et al. [44] first propose a self-supervised depth and motion framework minimizing the photometric consistency across a monocular video. Following this publication, many improvements have been proposed [40, 32, 17, 41, 1, 10, 36, 20, 39]. Wang et al. [40] incorporate a second-order gradient descent-based pose refinement module, into end-to-end training. Yang et al. [41] introduce joint optimization of depth and motion with normal and edge information to force additional geometric loss while preserving the edges. Mahjourian et al. [32] enforce the geometric consistency across reconstructed 3D points as well as the photometric consistency. Bian et al. [1] and Chen et al. [10] also impose the depth consistency loss by comparing multiple predicted depth, but they further estimate dynamic objects’ mask [1] or camera intrinsics [10]. Godard et al. [18] propose a minimum reprojection loss to handle occlusion robustly and a multi-scale sampling method to reduce artifacts. Ranjan et al. [36] introduce coordinated training frameworks composed of multiple neural networks for depth, camera motion, optical flow, and motion segmentation. Guizilini et al. [20] introduce a detail-preserving representation by learning representations that maximally propagate dense appearance and geometric information through 3D convolutions. Vasiljevic et al. [39] represent the depth with differentiable pixel-wise projection rays for learning with uncalibrated single viewpoint cameras. Recently, researches have been actively conducted to improve the performance of depth estimation in association with the semantic segmentation task. For instance, Klingner et al. [25] leverage semantic segmentation guidance to adaptively mask out the photometric inconsistency in dynamic scenes. Alternatively, Chen et al. [9] and Guizilini et al. [21] improve the performance of monocular depth estimation while enhancing semantic understanding by extracting features that are commonly related to semantics and geometry. They show that implicit feature learning through semantic prior knowledge can play an important role in 3D geometric perception.

2.2. Disentangling Camera and Object Motion

Disentangling local object motion from the global camera ego-motion is a key to improve the robustness of both depth and motion estimation in dynamic situations. Due to the motion ambiguity inherent to monocular-based techniques, most existing studies rely on stereo camera setup [6, 26]. This kind of system is advantageous in this context since metric scale depth (for each individual frame) coupled with semantic information (e.g., 2D objects’ bounding boxes [6] or segmentation labels [26]) offers privileged information to disentangle the ambiguity between the static background and the moving objects. While stereo-vision systems simplify the problem, solving this disentanglement using monocular cameras appears to be significantly more complex [19, 7, 25, 12, 28, 4]. Some of the works [7, 28] leverage instance segmentation map to estimate the motion field of individual objects. Casser et al. [7, 8] especially focus on designing a geometric structure in the learning process by modeling the scene and objects. Lee et al. [28, 27] focus on a geometrically correct
two-stage warping process that improves both photometric and geometric projection consistency in dynamic situations. Recent works attempt to disentangle the motion of objects with weaker semantic prior knowledge (e.g., from pixel-level to box-level prior). Brazil et al. [4] learn a 3D object bounding box with their orientation and 3D confidence from a monocular video. Gordon et al. [19] introduce a motion field representation with bounding box information to train depth, ego-motion, and dynamic motion from uncalibrated cameras. Li et al. [29] extend the motion field representation with a motion sparsity loss without additional semantic prior knowledge. Gao et al. [15] propose attentional motion networks to adaptively focus on each object and background feature without semantic priors.

3. Methodology

We introduce a two-stage pipeline for joint depth and motion learning. Our main objective is to disentangle the camera’s and objects’ motion in a self-supervised manner. In this section, we present the two projection stages composing our system, and the networks: DepthNet, and MotionNet with a shared encoder and two branch decoders. Further, we detail our dynamics attention module and contrastive sample consensus for modeling camera and object motions with the semantic guidance.

3.1. Two-Stage Motion Disentanglement

The overall schematic framework of the proposed method is illustrated in Fig. 2. The self-supervision of our architecture is achieved by warping the source frame $I_1$ to its adjacent target frame $I_2$, where $I \in \mathbb{R}^{3\times H \times W}$ is an RGB image sampled from a monocular video. The residual error resulting from this warping is used as a training signal.

**Stage 1 – depth and ego-motion:** We first predict each source and target view’s depth map ($D_1$, $D_2$) via our DepthNet $\mathcal{D}_\theta : \mathbb{R}^{3 \times H \times W} \rightarrow \mathbb{R}^{1 \times H \times W}$ with trainable parameters $\theta$. By concatenating two sequential images and depth maps ($I_1$, $D_1$, $I_2$, $D_2$) as an input, our proposed motion encoder $\mathcal{M}_\omega : \mathbb{R}^{8 \times H \times W} \rightarrow \mathbb{R}^{c_\omega \times h_\omega \times w_\omega}$ with trainable parameters $\omega$ extracts bottleneck motion features. Using the last layer’s bottleneck feature as an input for the ego-motion decoder $\mathcal{E}_\phi : \mathbb{R}^{c_\omega \times h_\omega \times w_\omega} \rightarrow \mathbb{R}^{6}$ with trainable parameters $\phi$, we estimate the six-dimensional (three translations and Euler angles) relative transformation vector $T_{ego}^{ego}$ as a forward camera ego-motion. We then synthesize the ego-warped image $I_{ego}^{ego}$ and its depth map $D_{ego}^{ego}$ as outputs of the first stage as

$$\left\{ \hat{I}_2^{ego}, \hat{D}_2^{ego} \right\} = \mathcal{F}_{wd}(I_1, D_1, T_{ego}^{ego}, K),$$

where $\mathcal{F}_{wd}$ is a forward projection function proposed in [28], and $K \in \mathbb{R}^{3 \times 3}$ is a given camera intrinsic matrix. We postulate that this ego-warped image and its projected depth are structurally aligned to the target view except for occluded and disoccluded regions if there are no moving objects.

**Stage 2 – residual motion field:** In the second projection stage, we residually predict a motion translation field. Since we synthesize the target view with the predicted camera motion, we conjecture that the misaligned regions are caused from local object motions. Using this clue, we model the object motion as a residual motion field $T^{res}$ using...
our motion encoder and a residual motion field decoder \(\mathcal{O}_\psi: \mathbb{R}^{c_1 \times h_1 \times w_2} \rightarrow \mathbb{R}^{3 \times H \times W}\) with trainable parameters \(\psi\). Specifically, we concatenate the outputs from the first projection stage and target frame’s image and depth \((I_2, D_2, I_3, D_3)\) as an input for the motion encoder. We again feed this to our motion encoder, and its output features are fed to the residual motion field decoder. This local object motion is represented only with a 3D translation field to reduce the rotation ambiguity from the camera. Finally, we compose the total motion field \(T^{\text{tot}} \in \mathbb{R}^{6 \times H \times W}\) from the predicted ego-motion\(^1\) and residual motion field through pixel-wise matrix multiplication. Given this total motion field, source image, and target depth map, we synthesize the final target image and its depth map as

\[
\{\hat{I}_2^{\text{tot}}, \hat{D}_2^{\text{tot}}\} = \mathcal{F}_{\text{inv}}(I_1, D_2, T_2^{\text{tot}} \rightarrow 1, K),
\]

where \(\mathcal{F}_{\text{inv}}\) is our pixel-wise inverse projection function. We optimize the whole frameworks by minimizing the photometric and geometric errors between \(\{I_2, D_2\}\) and \(\{\hat{I}_2^{\text{tot}}, \hat{D}_2^{\text{tot}}\}\). The loss functions will be discussed in Sec. 3.4.

### 3.2. Dynamics Attention Module

Since the camera motion and the residual motion field estimation are two complementary tasks, we postulate that using a shared encoder for these two tasks would improve their efficiency and the motion feature representation. To maximize this effect, we propose dynamics attention module (DAM) as described in Fig. 3. The encoding part of our unified motion networks is based on the ResNet-18 [22] structure. As an input for the networks, we concatenate two consecutive images and depth maps, which has eight channels in total. Motion features are learned while passing through each residual layer of the encoder. In this process, we attach DAM after the residual layers (ResLayer-2, -3, and -4) to selectively extract the ego-motion and residual motion features. We design DAM by referring to the generic self-attention structure that is transformed after context modeling introduced in GCNet [5]. To be specific, we first squeeze the channel dimension with two \(1 \times 1\) \textit{conv} layers and generate a spatial attention map via \textit{softmax} along the spatial dimension. This spatial attention is multiplied to the input feature, which represents a global attention pooling for context embedding. Then, with the reduction ratio set to \(r = 4\), the pooled feature is transformed with a bottleneck of two \(1 \times 1\) \textit{conv} layers. Finally, the transformed feature is added to the input feature in element-wise for feature fusion. This self-attention module is applied to each ego-motion and residual motion feature. If the motion feature is extracted to predict the camera motion, the ego-motion attention module is activated, and if estimating the residual motion field, we operate the residual motion

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\(^1\)Since the final warping is inverse direction, the direction of ego-motion also should be inverted, which is estimated by feeding a reverse-ordered input \((I_2, D_2, I_1, D_1)\) to the ego-motion networks.
3.3. Contrastive Sample Consensus

Motion variation issue While learning the residual motion field, our motion networks are trained to minimize the local errors triggered by an individual object motion. However, due to the limitation of self-supervisory optimization by photometric consistency, motion fluctuation\(^2\) occurs during training. As shown in Fig. 5, the discriminative regions, e.g., headlights, tend to be inferred with high motion response, while the homogeneous regions, e.g., windows, have relatively small motion. To mitigate this issue, we propose contrastive sample consensus (CSAC) to boost the motion consistency.

Motion regularization via CSAC Given a semantic prior as a 2D object box and its geometric prior (depth), we design a differentiable regularization module combining traditional random sampling and recent deep learning techniques. This regularization relies on two assumptions:

**Assumption 1 (geometric prior)** Each 2D detection box contains a potentially movable object, and it belongs to the foreground region.

**Assumption 2 (semantic prior)** The motion vectors in each box are distributed into two groups (background: small, object: large), and those belonging to the object group should converge to a single motion vector considering its rigidity under a short time period.

From these assumptions, we train the motions from the foreground and background by motion-repulsive embedding as introduced in Algorithm 1. In this algorithm, first we estimate the initial foreground mask from our predicted depth map on the detection box using [34] on the depth values (line 3). From this initial binary segmentation mask, we iteratively estimate the representative motion for the foreground and background through a random sampling technique. During the iteration, we measure the L1-norm between the hypothesis \(v_h\) and query vectors \(v_q\) for each translation axis, and calculate the inlier scores (line 10) as

\[
S = \sum_{v_q \in V} F_{\text{inlier}} \left( \left| \frac{v_h - v_q}{v_h} \right| \_1 \right),
\]

where \(F_{\text{inlier}}\) is designed as

\[
F_{\text{inlier}}(x) = 1 - \sigma(\alpha \cdot (x - \beta)),
\]

which is a soft inlier counting with a sigmoid function \(\sigma\), proposed by [2, 3]. In our case, \(\alpha\) and \(\beta\) are set to 30.0 and 0.2 respectively based on cross-validation. Then, we measure the iteration score \(S_i\) by simply aggregating the inlier scores to find the best hypothesis (line 11). The motion refinement is operated by multiplying the query vectors and inlier scores as weights (line 14). Note that these iterations are processed by the CPU since we do not require gradients for motion estimation. Once we get the refined motion vector \(\bar{v}\), we calculate the contrastive penalty loss (line 17), imposed for each foreground and background as

\[
\mathcal{L}_{\text{csac}} = \sum_{v_q \in V_f} \left\{ 1 - F_{\text{inlier}}(\max(0, (|\bar{v}_f| - |v_q|)/|\bar{v}_f|)) \right\},
\]

\[
\mathcal{L}_{\text{csac}}^b = \sum_{v_q \in V_b} \left\{ 1 - F_{\text{inlier}}(\max(0, (|v_b| - |\bar{v}_b|)/|v_b|)) \right\},
\]
we propose a multi-phase learning technique for efficient

Table 1. Assigned tasks for each phase are jointly trained. In

where $|\bar{v}_f|$ and $|\bar{v}_b|$ are the magnitudes of refined foreground and background motions respectively. This operation is processed by the GPU to perform the gradient propagation. In this equation, we penalize the foreground motions smaller than $|\bar{v}_f|$, and background motions larger than $|\bar{v}_b|$, in order to enhance motion contrast between the foreground and background, and this also meets our Assumption 2. Fig. 6 illustrates the importance of our motion contrast enhancement process to learn more accurate motion boundaries. Our final residual motion field regularization loss $\mathcal{L}_{mr}$ is the summation of $\mathcal{L}_{csac}^f$ and $\mathcal{L}_{csac}^b$ (per-box losses), and normalized to perform per-pixel loss for each mini-batch.

### 3.4. Training Scheme

**Multi-phase joint training** The proposed learning system is composed of complicated submodules. Although it is possible to gradually converge through end-to-end training, we propose a multi-phase learning technique for efficient and fast convergence. We summarize the training scheme in Table 1. Assigned tasks for each phase are jointly trained. In phase-1, since the residual motion branch is inactivated, we set the residual motion to be zero.

**Self-supervised objective** Our complete objective function is composed of phase-1 loss $\mathcal{L}^p_1$ and phase-2 loss $\mathcal{L}^p_2$ defined as

$$
\mathcal{L}^p_1 = \lambda_p \mathcal{L}_p + \lambda_g \mathcal{L}_g + \lambda_s \mathcal{L}_s + \lambda_h \mathcal{L}_h,
$$

$$
\mathcal{L}^p_2 = \lambda_{mr} \mathcal{L}_{mr} + \lambda_{ms} \mathcal{L}_{ms} + \lambda_{mp} \mathcal{L}_{mp} + \lambda_{mc} \mathcal{L}_{mc},
$$

where loss weights are grouped as $\lambda^{p1} = \{\lambda_p, \lambda_g, \lambda_s, \lambda_h\}$ and $\lambda^{p2} = \{\lambda_{mr}, \lambda_{ms}, \lambda_{mp}, \lambda_{mc}\}$, and each sub-loss is summarized as follows:

- $\mathcal{L}_p$ and $\mathcal{L}_g$: Photometric and geometric consistency losses defined in [1, 15]. Occluded and disoccluded regions are masked out by geometric inconsistency map [28]. We replace their global and object-wise motion transformation to our pixel-wise motion representation.

- $\mathcal{L}_s$: Generic edge-aware depth smoothness term, which is standardized in CC [36].

- $\mathcal{L}_h$: Object scale constraint loss with height prior, introduced in Struct2Depth [7]. We use box height as the prior.

- $\mathcal{L}_{ms}$: Proposed motion field regularization loss via CSAC. We newly propose a reparametrized edge-aware motion smoothness loss. Compared to the motion-repulsive embedding by our motion contrastive learning, we add motion-attractive embedding to merge the near motion vectors locally. To prevent blurry inference near object boundary, we reparametrize the gradient of the edges with $\tau$ as

$$
\mathcal{L}_{ms} = \sum (\nabla {\tau} \cdot e^{-|\nabla D|/\tau})^2,
$$

where we set $\tau = 0.1$ in our training.

- $\mathcal{L}_{mp}$ and $\mathcal{L}_{mc}$: Motion sparsity and consistency losses, which are introduced in [19, 29].

### 4. Experiments

In this section, we validate our proposed methods: DAM and CSAC. We report and analyze experimental results for the tasks of monocular depth and scene flow estimation, motion segmentation, and visual odometry. For the sake of fairness, all competing techniques are purely monocular, moreover, we rule out the impact of different network architectures, e.g., PackNet [20] and DispNet [44].

#### 4.1. Implementation Details

**Networks** We design DepthNet with ResNet18-based ImageNet [37] pretrained encoder and decoder structure. The decoder has the same structure as Monodepth2 [18], and its output is a single-scale inverse depth map with a sigmoid activation. For MotionNet, we use ImageNet pretrained ResNet18 encoder with DAM followed by two motion branches: ego-motion decoder with three convolutional layers, and residual motion field decoder proposed by Gordon et al. [19]. Each block of the motion field decoder refines the motion feature from the previous block concatenated with its symmetrically corresponding output feature from the encoding block.

**Training** Our system is implemented in PyTorch [35] and trained using the ADAM optimizer [24] with the initial learning rate of $10^{-4}$, $\beta_1 = 0.9$, and $\beta_2 = 0.999$ on 2×Nvidia
which produces a better motion feature representation. Sec-
weights, \( \Lambda \) (90%) and validation (10%) sets are randomly split from
Table 2, we achieve better performance with fewer number of
Numbers are reported after phase-3. Using a single motion encoder yields better performance on monocular depth estimation with fewer parameters.

| Models          | DAM | CSAC | phase-1 | phase-3 |
|-----------------|-----|------|---------|---------|
|                 |     |      | all     | obj     | all     | obj     |
| A1              | –   | –    | 0.126   | 0.202   | 0.120   | 0.199   |
| A2              | –   | ✓    |         |         | 0.113   | 0.190   |
| A3              | ✓   | –    | 0.121   | 0.196   | 0.109   | 0.182   |
| A4              | ✓   | ✓    |         |         |         |         |

Table 3. Ablation study on DAM and CSAC. We measure AbsRel errors after phase-1 and phase-3 on both all and obj areas.

RTX 2080 GPUs. We set the mini-batch size to 4 and each epoch is trained with 1,000 randomly sampled sequences following the augmentation policy of SC-SfM [1]. We train phase-1 and phase-2 for 10 epochs respectively. The loss weights, \( \lambda^p \) and \( \lambda^o \), are tuned differently depending on the dataset and training phase. We describe this in detail in the supplement. To be brief, we empirically found that every objective shows stable convergence when the magnitude of each weighted per-pixel loss \( (\lambda L_p) \) is 0.05 times the weighted photometric loss \( (\lambda x) \). Dataset Our system is trained and validated in KITTI [16], Cityscapes [11], and Waymo Open Dataset [38]. For KITTI and Cityscapes, we utilize the VIS annotations [28] for testing motion segmentation, and detection prior in CSAC training with a random margin up to 10% for generating detection box. The input resolution is set to 832 × 256 for KITTI and Cityscapes, and 480 × 320 for Waymo Open Dataset.

4.2. Ablation Study

To quantify the impact of our motion encoding using DAM and the motion regularization via CSAC, we propose various ablation studies. In this experiment, the training (90%) and validation (10%) sets are randomly split from KITTI raw monocular videos. We repeat the training 5 times and average the performance of monocular depth estimation. First, we perform an ablation to verify our motivation on sharing the motion encoder for MotionNet, while estimating the camera and object motion at the same time. As shown in Table 2, we achieve better performance with fewer number of trainable parameters, compared to the model with separated encoders. We, thus, conclude that our invertible attention mechanism enhances the capability of motion disentangling, which produces a better motion feature representation. Second, we proceed ablation integrated with both DAM and CSAC. In this case, we measure AbsRel error on both entire (all) and object (obj) regions. As demonstrated in Table 3, we conduct four ablations (A1~A4) according to our proposed models. We observe that in phase-1, feature extraction with DAM (A3 and A4) has a marginal improvement on depth estimation. After training MotionNet with residual motion field (phase-2), we notice a significant improvement while refining the depth in phase-3. In addition, regularization through CSAC further improves the depth estimation on the object area by providing a rigid body constraint. We conclude that our modules play an important role in enhancing the performance of joint depth and motion estimation.

4.3. Monocular Scene Flow Estimation

To validate our pixel-wise motion and depth estimation simultaneously, we assessed our monocular scene flow estimation on the KITTI Scene Flow 2015 training set, as shown in Table 4. We compare our method with existing monocular-based training methods. Compared to the methods not using semantic priors, we achieve more than 57.8% accuracy gain for estimating the disparity of objects on the target image (D2-fg). Despite using weaker priors, we obtain competitive results against techniques relying on strong semantic prior, such as, Insta-DM [28].

4.4. Motion Segmentation

We demonstrate object motion segmentation on KITTI Scene Flow 2015 training set and Cityscapes with VIS annotation [28]. This is enabled by leveraging inlier scores (threshold of 0.5) of the best hypothesis, as designed in Eq. (4). Table 5 demonstrates that our regularization with contrastive learning based on the geometric prior significantly improves the performance of semantic perception task. We demonstrate qualitative results in Fig. 7.

4.5. Monocular Depth Estimation and Visual Odometry

Finally, we provide comparisons to state-of-the-arts [18, 29, 7, 19, 25] of self-supervised monocular depth and
Table 7. Relative translation $t_{err}$ (%) and rotation $r_{err}$ (°/100m) errors on KITTI-VO.

| Method | Seq. 09 | Seq. 10 |
|--------|---------|---------|
| Ours (w/ DAM) | 8.9 | 9.5 | 4.7 |
| Ours (w/o DAM) | 9.7 | 3.4 | 9.9 | 4.3 |

Table 8. Relative translation $t_{err}$ (%) and rotation $r_{err}$ (°/100m) errors on KITTI-VO.

| Method | Seq. 09 | Seq. 10 |
|--------|---------|---------|
| Ours (w/ DAM) | 8.9 | 9.5 | 4.7 |
| Ours (w/o DAM) | 9.7 | 3.4 | 9.9 | 4.3 |

5. Conclusion

We proposed a novel self-supervised learning framework to estimate the motion field of a dynamic scene from a monocular camera. First, our approach heavily relies on a novel attention module dedicated to the disentanglement of the camera ego-motion and the objects’ motions, which has proven to be effective to improve the overall performance of our network. Second, we designed an object motion field estimation through contrastive sample consensus.

With given geometric and semantic priors, we leverage a motion-repulsive embedding near object motion boundaries to estimate more accurate motion field. The effectiveness of our system has been demonstrated on various driving datasets. One remaining limitation is the rigid body assumption of the moving objects. While our approach is suitable for a traffic scene containing vehicles, it is not appropriate for deformable objects such as pedestrians. Therefore, we leave this problem as our future direction to improve the applicability of the technique to more diverse scenarios.

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Supplementary Material

In this supplementary material, we present additional details on the models, training scheme, and experiments that could not be included in the main text due to space constraints. All tables, figures, equations, and references in this supplementary file are self-contained.

Contents of the supplementary material The supplementary material is composed of the following. (1) Details of our models. (2) Additional ablation study such as networks design and hyper-parameter settings. (3) Additional experimental results.

A1. Details of Architectures

The detailed architectures of DepthNet, DAM, and MotionNet are specified in Table A1, Table A2, and Table A3, respectively. Generic layers, e.g., conv, fc, pool, etc., are specified starting with a lowercase letter. Nonlinear activation functions, e.g., ReLU, ELU, etc., are abbreviated for visibility. The encoders of DepthNet and MotionNet are both based on ResNet18 [4]. We declare the residual block as ResBlock for each encoder.

DepthNet For the decoder of DepthNet, we adopt the structure of MonoDepth2 [2]. DepthNet can predict depth maps with five scales, but we empirically found that single-scale training produces better performance than multi-scale training. Thus, we predict the depth map from the last layer of the decoder, which is activated with a sigmoid function.

MotionNet with DAM For DAM, we design the weighted context and transforming operation for each ego-motion and residual motion feature, respectively. We attach DAM after the 2nd, 3rd, and 4th residual layer in the ResNet encoder of MotionNet. In the case of the ResNet18 encoder, each residual layer is composed of two residual blocks. GCNet [1] attached the attention module to each residual block, however, we empirically found that deploying DAM only after the residual layer leads to a better trade off between performance and computational time. The details of this ablation is specified in Sec. A2 and examples of the spatial attention map are visualized in Sec. A3. The decoder of MotionNet has multiple refining steps, which has been proposed by Gordon et al. [3]. Every refinement step aggregates the features from the encoding layer and predictions from the lower layer. Similar to DepthNet, we predict the residual motion field with a single-scale, which is refined from the last layer of the decoder.

A2. Additional Ablation Study

In this section, we discuss additional ablation studies of different design choices and hyper-parameter settings. We follow the same configurations of experiments, e.g., dataset and training scheme, which are described in Sec. 4.2. of our main paper.

Different positional configurations of DAM As discussed in the previous section, there are two configuration options where to deploy DAM in the encoder of MotionNet: DAM after every residual block (GCNet [1] style), and (b) after the last residual block in each residual layer.

Figure A1. Different positional design options for DAM in a residual layer. We validate two design choices for DAM: (a) after every residual block (GCNet [1] style), and (b) after the last residual block in each residual layer.

Figure A2. Trends of motion field consistency loss in phase-2 for different DAM configurations. We train MotionNet on the KITTI dataset from scratch, and plot its training loss.

Figure A3. Validation error trends in phase-1 depending on the presence or absence of DAM in the motion encoder. Models are trained and tested on the KITTI dataset, and we measure the AbsRel errors on both all and object areas.
however, to see distinctive results, we train MotionNet from random initialization with DepthNet pretrained from phase-1. The results show that the configuration with DAM after the last ResBlock converges fastest. From these ablation studies, we conjecture that the positional configuration of DAM has a relation with model complexity. Since the shared motion encoder performs two tasks, there could be a confusion from different self-supervisory signals. DAM helps to switch the extraction of motion feature in the encoder, however, the convergence will become slow if this switching mechanism is too complicated. Therefore, considering the training efficiency, we have chosen the configuration of DAM after the last ResBlock. Finally, we analyse the convergence trends of the networks in phase-1 with and without DAM in Fig. A3 – applied on the objects only and on the entire image. We can notice a marginal improvement of the depth quality when
| Type          | Name          | Kernel | Stride | Channel I/O | In. resol. | Out. resol. | Input          |
|--------------|---------------|--------|--------|-------------|------------|-------------|----------------|
| Encoder      | conv_0        | 7 x 7  | 2      | (3,1,1)/64  | 256 x 832  | 128 x 416   | images, depth maps |
|              | maxpool_1     | 3 x 3  | 2      | 64/64       | 128 x 416   | 64 x 208    | conv_0         |
|              | ResBlock_1.a  | –      | 1      | 64/64       | 64 x 208    | 64 x 208    | maxpool_1      |
|              | ResBlock_1.b  | –      | 1      | 64/64       | 64 x 208    | 64 x 208    | ResBlock_1.a   |
|              | ResBlock_2.a  | –      | 2      | 64/128      | 64 x 208    | 32 x 104    | ResBlock_1.b   |
|              | ResBlock_2.b  | –      | 2      | 1/128/128   | 32 x 104    | 32 x 104    | ResBlock_2.a   |
|              | DAM_2         | –      | 1      | 128/128     | 32 x 104    | 32 x 104    | ResBlock_2.b   |
|              | ResBlock_3.a  | –      | 2      | 128/256     | 32 x 104    | 16 x 52     | DAM_2          |
|              | ResBlock_3.b  | –      | 1      | 256/256     | 16 x 52     | 16 x 52     | ResBlock_3.a   |
|              | DAM_3         | –      | 1      | 256/256     | 16 x 52     | 16 x 52     | ResBlock_3.b   |
|              | ResBlock_4.a  | –      | 2      | 256/512     | 16 x 52     | 8 x 26      | DAM_3          |
|              | ResBlock_4.b  | –      | 1      | 512/512     | 8 x 26      | 8 x 26      | ResBlock_4.a   |
|              | DAM_4         | –      | 1      | 512/512     | 8 x 26      | 8 x 26      | ResBlock_4.b   |
|              | conv_1        | 1 x 1  | 1      | 512/256     | 8 x 26      | 8 x 26      | DAM_4          |
|              | conv_2        | –      | 2      | 256/256     | 8 x 26      | 8 x 26      | conv_1         |
|              | conv_3        | 3 x 3  | 1      | 256/256     | 8 x 26      | 8 x 26      | conv_2         |
|              | conv_4        | 1 x 1  | 1      | 256/66      | 8 x 26      | 8 x 26      | conv_3         |
|              | avgpool       | –      | –      | 6/6         | 8 x 26      | 1 x 1       | conv_4         |
| Ego-motion   | mofconv_0     | 1 x 1  | 1      | 512/3       | 8 x 26      | 8 x 26      | DAM_4          |
| decoder      | concat_1.a    | 3 x 3  | 1      | 515/512     | 8 x 26      | 8 x 26      | mofconv_0, DAM_4 |
|              | conv_1.a      | 3 x 3  | 1      | 151/512     | 8 x 26      | 8 x 26      | concat_1.a     |
|              | conv_1.b      | 3 x 3  | 1      | 515/512     | 8 x 26      | 8 x 26      | concat_1.b     |
|              | concat_1.a    | –      | –      | (512,512)/1024 | 8 x 26     | 8 x 26      | concat_1.a, conv_1.b |
|              | mofconv_1     | 1 x 1  | 1      | 1024/3      | 8 x 26      | 8 x 26      | concat_1.a     |
|              | sum_1         | –      | –      | (3,3)/3     | 8 x 26      | 8 x 26      | mofconv_0, mofconv_1 |
| Res-motion   | upsample_3.a  | –      | –      | 3/3         | 8 x 26      | 16 x 52     | sum_1          |
|              | concat_3.a    | 3 x 3  | 1      | (3,128)/131 | 32 x 104    | 32 x 104    | upsample_3, DAM_2 |
|              | conv_3.a      | 3 x 3  | 1      | 131/128     | 32 x 104    | 32 x 104    | concat_3.a     |
|              | conv_3.b      | 3 x 3  | 1      | 131/128     | 32 x 104    | 32 x 104    | concat_3.a     |
|              | concat_3.a    | –      | –      | (128,128)/256 | 32 x 104  | 32 x 104    | concat_3.a, conv_3.b |
|              | mofconv_3     | 1 x 1  | 1      | 256/3       | 32 x 104    | 32 x 104    | concat_3.a     |
|              | sum_3         | –      | –      | (3,3)/3     | 32 x 104    | 32 x 104    | mofconv_3, concat_3.a |
| decoder      | upsample_4.a  | –      | –      | 3/3         | 32 x 104    | 64 x 208    | sum_3          |
|              | concat_4.a    | 3 x 3  | 1      | (3,64)/67   | 64 x 208    | 64 x 208    | upsample_4, ResBlock_1.a |
|              | conv_4.a      | 3 x 3  | 1      | 67/64       | 64 x 208    | 64 x 208    | concat_4.a     |
|              | conv_4.b      | 3 x 3  | 1      | 67/64       | 64 x 208    | 64 x 208    | concat_4.a     |
|              | concat_4.a    | –      | –      | (64,64)/128 | 64 x 208    | 64 x 208    | concat_4.a, conv_4.a |
|              | mofconv_4     | 1 x 1  | 1      | 128/3       | 64 x 208    | 64 x 208    | concat_4.a     |
|              | sum_4         | –      | –      | (3,3)/3     | 64 x 208    | 64 x 208    | mofconv_4, upsample_4 |
|              | upsample_5.a  | –      | –      | 3/3         | 32 x 104    | 128 x 416   | sum_3          |
|              | concat_5.a    | 3 x 3  | 1      | 3/67        | 128 x 416   | 128 x 416   | upsample_5, conv_0 |
|              | conv_5.a      | 3 x 3  | 1      | 128/416     | 128 x 416   | 128 x 416   | concat_5.a     |
|              | conv_5.b      | 3 x 3  | 1      | 128/416     | 128 x 416   | 128 x 416   | concat_5.a     |
|              | concat_5.a    | –      | –      | 6/128/128   | 128 x 416   | 128 x 416   | concat_5.a, conv_5.b |
|              | mofconv_5     | 1 x 1  | 1      | 128/3       | 128 x 416   | 128 x 416   | concat_5.a     |
|              | sum_5         | –      | –      | (3,3)/3     | 128 x 416   | 128 x 416   | mofconv_5, upsample_5 |
|              | upsample_6.a  | –      | –      | 3/3         | 128 x 416   | 256 x 832   | sum_4          |
|              | concat_6.a    | 3 x 3  | 1      | (3,3,1,1)/11 | 256 x 832  | 256 x 832  | upsample_6, images, depth maps |
|              | conv_6.a      | 3 x 3  | 1      | 11/8        | 256 x 832   | 256 x 832   | conv_6.a       |
|              | conv_6.b      | 3 x 3  | 1      | 11/8        | 256 x 832   | 256 x 832   | conv_6.a       |
|              | concat_6.a    | –      | –      | (8,8)/16    | 256 x 832   | 256 x 832   | conv_6.a, conv_6.b |
|              | mofconv_6     | 1 x 1  | 1      | 16/3        | 256 x 832   | 256 x 832   | conv_6.a       |
|              | sum_6         | –      | –      | (3,3)/3     | 256 x 832   | 256 x 832   | mofconv_6, upsample_6 |

Table A3. Details of MotionNet.
Table A4. Ablation study on different positional configurations of DAM. We follow the same ablation scheme of Sec. 4.2. in our main paper, and measure the AbsRel errors after phase-1 and phase-3 on both all and obj areas. In phase-3, we regularize the residual motion field with CSAC.

| Models                  | phase-1 | phase-3 |
|-------------------------|---------|---------|
|                          | all     | obj     | all     | obj     |
| without DAM             | 0.126   | 0.202   | 0.113   | 0.190   |
| DAM after every ResBlock| 0.122   | 0.199   | 0.111   | 0.181   |
| DAM after the last ResBlock | 0.121 | 0.196   | 0.109   | 0.182   |

Figure A4. Different inlier score mapping with $\alpha$ and $\beta$. The steeper the curve, the more discretized, so we conduct ablations to find appropriate values.

| $\{\alpha, \beta\}$ | D1 ($\gamma$) | D2 ($\gamma$) |
|----------------------|---------------|---------------|
| $\{50, 0.1\}$       | 34.1          | 41.3          |
| $\{30, 0.2\}$       | 32.5          | 35.7          |
| $\{10, 0.5\}$       | 33.8          | 37.2          |

Figure A5. Reparameterized gradient maps $e^{-VD/\tau}$ depending on different $\tau$. We visualize image, its depth map, and gradients over the $x$ and $y$ axis. Smaller value of $\tau$ reduces gradients on the edges.

Table A7. Summarization of loss weights for each phase.

| Phase | $\lambda_\text{mr}$ | $\lambda_\text{mc}$ | $\lambda_\text{ms}$ | $\lambda_\text{mp}$ | $\lambda_\text{mr}$ | $\lambda_\text{mc}$ | $\lambda_\text{ms}$ | $\lambda_\text{mp}$ |
|-------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|
| phase-1 | 1.0 | 1.0 | 0.1 | 0.2 | -- | -- | -- | -- |
| phase-2 | 1.0 | 1.0 | 0.1 | 0.2 | -- | 1.0 | 0.5 | 0.001 |
| phase-3 | 1.0 | 1.0 | 0.1 | 0.2 | 0.2 | 1.0 | 1.0 | 0.001 |

Table A8. Ablation study of different loss weights, $\lambda_\text{mr}$ and $\lambda_\text{ms}$, on the KITTI dataset. We measure the AbsRel errors on both all and obj areas.

Different $\alpha$ and $\beta$ for inlier score In Fig. A4, we visualize different mapping of the soft inlier score function $\mathcal{F}_\text{inlier}$ according to $\alpha$ and $\beta$ to analyze their impacts. The graph shows that a high $\alpha$ value makes the curve sharp, and this leads to increase the discretization of the inlier scores. In Table A5, we conduct an ablation study to find the appropriate values of $\alpha$ and $\beta$. From the results, we conclude that both high discretization and tolerant mapping have adverse effects on residual motion learning. As a result of this ablation study, we selected $\alpha = 30$ and $\beta = 0.2$ for CSAC.

Reparameterized edge-aware motion smoothness We visualize the reparameterized gradients maps according to different $\tau$ in Fig. A5. The vanilla edge-aware smoothness term ($\tau = 1.0$) is not distinctive enough to leverage the boundary prior of objects. By reparameterizing with a small value of $\tau$, we conjecture that the motion segmentation near the boundary of objects would be improved. We show motion segmentation results on different $\tau$ in Table A6.

DAM is employed. It underlines that during this training phase the motion encoder design only has little influence on the depth estimation. However, as underlined by other tests, DAM provides significant improvements on the overall system after the entire training process.

Configuration of loss weights We summarize the learning parameters for each dataset in Table A7. The photometric loss, $\mathcal{L}_p$, is defined as follows:

$$\mathcal{L}_p = \sum (\gamma_1 |I - \hat{I}|_1 + \gamma_2 (1 - \text{SSIM}(I, \hat{I})))$$  \hspace{0.5cm} (A8)$$

where $\text{SSIM}$ is the structural similarity loss [5], and $\{\gamma_1, \gamma_2\}$ is set to $\{0.3, 1.5\}$ based on cross-validation. Other parameters of our loss functions are the same as previous works as described in Sec. 3.4. of our main paper.

Different loss weights of $\lambda_\text{mr}$ and $\lambda_\text{ms}$. To justify the parametrization of the hyper-parameters $\lambda_\text{mr}$ and $\lambda_\text{ms}$, we propose another ablation study conducted on the KITTI dataset. For this experiment, we follow the training scheme and dataset described in Sec. 4.2. of our main paper. As
provided in Table A8, our motion regularization with CSAC shows stable training with $\lambda_{mr} = 0.2$ and $\lambda_{ms} = 1.0$.

### A3. Additional Experimental Results

In this section, we present additional experimental results as an extension of Sec. 4. of our main paper.  

**Full table of monocular depth estimation** We provide the full results of our models for the task of monocular depth estimation in Table A9. The results consistently show that our proposed modules, DAM and CSAC, favorably work on three different dataset: KITTI, Cityscapes, and Waymo Open Dataset.  

**Qualitative results** In addition to Fig. 7 in our main paper, we visualize the depth map and residual motion field in Fig. A6 and Fig. A7. Fig. A8 shows two representative effects of the regularization through CSAC: sharpen boundaries of object’s motion, and motion hole filling in the homogeneous areas. Our module consistently preserves the shape of the moving objects, while the baseline model distorts the appearance of objects.

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| Method          | Phase | Training | Test | Error metric ↓ | Accuracy metric ↑ |
|-----------------|-------|----------|------|----------------|------------------|
|                 |       |          |      | AbsRel SqRel RMSE RMSE log | \(\delta < 1.25\) | \(\delta < 1.25\) | \(\delta < 1.25\) |
| Baseline        | phase-1 | K  | K    | 0.126 0.975 5.244 0.211 | 0.849 0.946 0.979 |
| Ours (DAM)      | phase-1 | K  | K    | 0.123 0.920 5.212 0.205 | 0.854 0.945 0.978 |
| Ours (DAM)      | phase-3 | K  | K    | 0.120 0.895 4.972 0.196 | 0.859 0.950 0.980 |
| Ours (DAM+CSAC) | phase-3 | K  | K    | 0.114 0.876 4.715 0.191 | 0.872 0.955 0.981 |
| Baseline        | phase-1 | C+K | K    | 0.122 0.907 4.985 0.207 | 0.862 0.953 0.980 |
| Ours (DAM)      | phase-1 | C+K | K    | 0.119 0.883 5.021 0.206 | 0.861 0.954 0.979 |
| Ours (DAM)      | phase-3 | C+K | K    | 0.116 0.845 4.790 0.194 | 0.868 0.957 0.979 |
| Ours (DAM+CSAC) | phase-3 | C+K | K    | 0.111 0.805 4.708 0.187 | 0.875 0.962 0.981 |
| Baseline        | phase-1 | C  | C    | 0.128 1.322 6.942 0.198 | 0.833 0.949 0.978 |
| Ours (DAM)      | phase-1 | C  | C    | 0.127 1.330 6.903 0.196 | 0.838 0.950 0.979 |
| Ours (DAM)      | phase-3 | C  | C    | 0.124 1.281 6.818 0.189 | 0.849 0.951 0.981 |
| Ours (DAM+CSAC) | phase-3 | C  | C    | 0.116 1.213 6.695 0.186 | 0.852 0.951 0.982 |
| Baseline        | phase-1 | W  | W    | 0.161 1.724 7.825 0.217 | – – – |
| Ours (DAM)      | phase-1 | W  | W    | 0.159 1.707 7.816 0.215 | – – – |
| Ours (DAM)      | phase-3 | W  | W    | 0.155 1.692 7.448 0.212 | – – – |
| Ours (DAM+CSAC) | phase-3 | W  | W    | 0.148 1.686 7.420 0.210 | – – – |

Table A9. **Full results of our models for monocular depth estimation on KITTI (K) Eigen test set, Cityscapes (C) test set, and Waymo Open Dataset (W).** The models pretrained on Cityscapes and fine-tuned on KITTI are denoted by ‘C+K’. For each partition, **Bold**: Best.

**KITTI**

![KITTI](image1.png)

**Cityscapes**

![Cityscapes](image2.png)

(a) target image  (b) depth map  (c) residual motion field

(d) object box image and its inliers

Figure A6. **Qualitative results of depth and residual motion estimation in KITTI and Cityscapes.** The residual motion field is mapped into the HSV color space.
Figure A7. **Qualitative results of depth map and bidirectional residual motion field in Waymo Open Dataset.** AbsRel errors on all / obj: (b) 0.154 / 0.328, (c) 0.149 / 0.250 (improved distinction between obj and background), (d) 0.135 / 0.164 (sharpen object boundary). (e) Result of a diverged depth map, if auto-masking proposed by MonoDepth2 [2] fails. (f) Results of residual motion field for pedestrians.

Figure A8. **Qualitative results of motion inliers in Cityscapes.** CSAC makes the motion boundaries more clear and sharper as shown in the first row, and the motion holes in homogeneous regions more consistent on the rigid objects as demonstrated in the second row.