The effect of stellar evolution on SiC dust grain sizes

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ABSTRACT

Stars on the asymptotic giant branch (AGB) produce dust in their circumstellar shells. The nature of the dust-forming environment is influenced by the evolution of the stars, in terms of both chemistry and density, leading to an evolution in the nature of the dust that is produced. Carbon-rich AGB stars are known to produce silicon carbide (SiC). Furthermore, observations of the \( \sim 11\mu m \) SiC feature show that the spectral features change in a sequence that correlates with stellar evolution. We present new infrared spectra of amorphous SiC and show that the \( \sim 9\mu m \) feature seen in both emission and absorption, and correlated with trends in the \( \sim 11\mu m \) feature, may be due to either amorphous SiC or to nano-crystalline diamond with a high proportion of Si substituting for C. Furthermore, we identify SiC absorption in three ISO spectra of extreme carbon stars, in addition to the four presented by Speck et al. (1997). An accurate description of the sequence in the IR spectra of carbon stars requires accounting for both SiC emission and absorption features. This level of detail is needed to infer the role of dust in evolution of carbon stars. Previous attempts to find a sequence in the infrared spectra of carbon stars considered SiC emission features, while neglecting SiC absorption features, leading to an interpretation of the sequence inadequately describes the role of dust. We show that the evolutionary sequence in carbon star spectra is consistent with a grain size evolution, such that dust grains get progressively smaller as the star evolves. The evolution of the grain sizes provides a natural explanation for the shift of the \( \sim 11\mu m \) SiC feature in emission and in absorption. Further evidence for this scenario is seen in both post-AGB star spectra and in meteoritic studies of presolar grains.

Subject headings: infrared: stars — stars: carbon — circumstellar matter — dust
1. Introduction

1.1. Evolution during the Asymptotic Giant Branch (AGB) phase

Stars in the mass range 1-8 M$_\odot$ eventually evolve up the asymptotic giant branch (AGB) where they begin to lose mass and form circumstellar shells of dust and gas. During their ascent of the AGB, mass-loss rates are expected to increase with the luminosity of the star, resulting in progressive optical thickening of circumstellar shells. Furthermore, the chemistry of these stars’ atmospheres, and thus of their circumstellar shells, changes as a result of dredge-up of newly formed carbon from the He-burning shell. Due to the extreme ease of formation and stability of CO molecules, the chemistry in circumstellar shells is controlled by the C/O ratio. If C/O $< 1$ all the carbon is trapped in CO, leaving oxygen to dominate the chemistry. Conversely, if C/O $> 1$ all the oxygen is trapped in CO, and carbon dominates the chemistry. Stars start their lives with cosmic C/O ratios ($\approx 0.4$), and are thus oxygen-rich. In some AGB stars, the dredge-up of newly formed carbon is efficient enough to raise the C/O above unity, and these stars are known as carbon stars. They are expected to have circumstellar shells dominated by amorphous or graphitic carbon grains, although other dust grains are also important (e.g. silicon carbide; SiC).

As the mass-loss rate increases with the evolution of the AGB stars, the dust shells get thicker (both optically and geometrically) and these stars eventually become invisible at optical wavelengths and very bright in the infrared (IR). Such stars are known as “extreme carbon stars” (Volk et al. 1992, 2000). At this stage, intense mass loss depletes the remaining hydrogen in the star’s outer envelope, and terminates the AGB. Up to this point the star has been making and dredging-up carbon, thus these shells have even more carbon available for dust production than optically bright (early) carbon stars (i.e. the Si/C ratio decreases with the evolution of these stars). The rapid depletion of material from the outer envelope of the star means that this extremely high mass-loss phase must have a relatively short duration (a few $\times 10^4$ years; Volk et al. 2000).

1.2. Post-AGB evolution

Once the AGB star has exhausted its outer envelope, the AGB phase ends. During this phase the mass loss virtually stops, and the circumstellar shell begins to drift away from the star. At the same time, the central star begins to shrink and heat up from 3000 K until it is hot enough to ionize the surrounding gas, at which point the object becomes a planetary nebula (PN). The short-lived post-AGB phase, as the star evolves toward to the PN phase, is also known as the proto-planetary nebula (PPN) phase. The detached dust shell drifts away
from the central star causing a PPN to have cool infrared colors from its cooling dust shell. Meanwhile, the optical depth of the dust shell decreases as it expands allowing the central star to be seen and making such objects optically bright. The effect of decreasing optical depth and cooling dust temperatures changes the spectrum of the circumstellar envelope, revealing features that were hidden during the AGB phase.

1.3. Observing dust around carbon stars

Circumstellar shells of carbon stars are expected to be dominated by amorphous or graphitic carbon grains. These dust species do not have diagnostic infrared features and merely contribute to the dust continuum emission. However, silicon carbide (SiC) does exhibit a strong infrared feature, which can be exploited when studying carbon stars.

In the context of stardust, SiC has been of great interest since its formation was predicted by condensation models for carbon-rich circumstellar regions (e.g. Friedemann 1969; Gilman 1969). Gilra (1971, 1972) predicted that SiC should re-emit absorbed radiation as a feature in the 10–13\(\mu m\) region. Following these predictions, a broad infrared (IR) emission feature at \(\sim 11.4\mu m\) that is observed in the spectra of many carbon stars has been attributed to solid SiC particles (e.g. Hackwell 1972; Treffers & Cohen 1974). Indeed, SiC is now believed to be a significant constituent of the dust around carbon stars. Although Goebel et al. (1995) and Clément et al. (2003) adopted the name 11+\(\mu m\) feature to reflect the variation in observed peak positions in astronomical spectra, this implies that the features always occur longward of 11\(\mu m\). We have adopted \(\sim 11\mu m\) to reflect the variations in peak positions of this feature.

The effect of the evolution of the density of the dust shell on observed features, and particularly on the \(\sim 11\mu m\) feature, have been discussed extensively (e.g. Cohen 1984; Baron et al. 1987; Willem 1988; Chan & Kwok 1990; Goebel et al. 1995; Speck et al. 1997; Sloan et al. 1998, see § 3.1). Not all these previous works agree. All studies concur that the increasing optical depth leads to decreasing color temperatures from the stars as the stellar photosphere becomes hidden from view, and the dust from which we receive light becomes progressively cooler. At the same time, the \(\sim 11\mu m\) feature tends to become weaker (relative to the continuum) and flatter topped (less sharp peaked) and possibly broader. Various explanations of this behavior have been proposed, but none are entirely satisfactory. Initially the diminution of the \(\sim 11\mu m\) feature was attributed to coating of the grains by amorphous carbon (e.g. Baron et al. 1987; Chan & Kwok 1990). However, meteoritic data does not support this hypothesis (see § 1.4). Moreover, more recent studies of the \(\sim 11\mu m\) feature have shown that it is consistent with SiC self-absorption, i.e. absorption by cooler SiC
particles, located in the outer part of the dust shell, where they can absorb the SiC emission feature produced by warmer SiC closer to the central star (Speck et al. 1997). Indeed, Speck et al. (1997) showed that every star in their sample whose underlying continuum temperature ($T_{\text{col}} < 1200$ K) was best fitted by self-absorbed SiC, whether the $\sim 11\mu$m feature was in net emission or net absorption. As the dust shell reaches extreme optical depths, the $\sim 11\mu$m feature will eventually be seen in net absorption. However, these absorption features are rare and have mostly been ignored in discussions of evolutionary sequences in carbon star spectra.

1.4. Meteoritic Evidence

Silicon carbide is an important presolar grain found in meteorites. The isotopic compositions of presolar grains indicate that they originated outside the solar system. Presolar SiC was first discovered by Bernatowicz et al. (1987) and since then has been the focus of a great deal of laboratory work (see Bernatowicz et al. 2005, and references therein). The most important findings of this work are: (1) most of the SiC presolar grains were formed around carbon stars; (2) nearly all ($\sim 90\%$) are of the cubic $\beta$-polytype$^1$; (3) with one exception, SiC grains are never found in the cores of carbon presolar grains (unlike other carbides - TiC, ZrC, MoC); (4) the grain-size distribution is large (1.5nm to 26$\mu$m), with most grains in the $0.1 - 1\mu$m range, but with single-crystal grains can exceed 20$\mu$m in size.

Observations of the $\sim 11\mu$m feature have been compared with laboratory spectra of various forms of SiC and after some false starts, has now been attributed to $\beta$-SiC, matching the information retrieved from meteoritic samples (Speck et al. 1999; Clément et al. 2003). However, there are still some discrepancies between observational and meteoritic evidence (most notably related to grain size). Studies of meteoritic SiC grains can aid our understanding of their evolution.

1.5. Purpose

The goal of this paper is to extract the evolution of the dust from the infrared spectra of carbon-rich AGB stars (both optically bright and “extreme”) and post-AGB stars. In § 2

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$^1$Silicon carbide can form into numerous different crystal structures, known as polytypes. $\beta$-SiC is the cubic polytype, and is now believed to be the dominant form of SiC forming around carbon stars; see § 1.4, and Speck et al. (1997, 1999); Daulton et al. (2003)
we present new infrared spectra of amorphous silicon carbide which may explain some of the features seen in the carbon star spectral sequences. In § 3 we review studies of the infrared spectra of carbon stars which demonstrate the changes in spectral features associated with stellar evolution. We also present new detections of \( \sim 11 \mu \text{m} \) absorption features in extreme carbon stars, which are essential to our understanding of the dust grain evolution. In § 4 we present a dust evolution sequence to explain the spectral changes in carbon stars. The summary and conclusions are in § 5.

2. New spectra of amorphous silicon carbide

2.1. Experimental samples and techniques

Superior Graphite donated the bulk β-SiC. The purity is 99.8%. Bulk α-SiC (purity = 99.8%) in the 6H polytype was purchased from Alfa/Aesar (Lot # c19b06). Grain size varied from 1 to 25 \( \mu \text{m} \). Nanocrystals of 2-5 nm size produced by gas-phase combustion (Axelbaum et al. 1996) best matches the X-ray diffraction pattern of β-SiC but contains some 6H as well (for details see Hofmeister et al. 2000). This sample may also contain SiC in the diamond structure, as synthesized by Kimura & Kaito (2003) and discussed further below. We designate this sample as “nano \( \beta + \alpha \)”. These three samples were studied by Speck et al. (1999) and Speck & Hofmeister (2004). Nanocrystals were also purchased from Nanostructured and Amorphous Materials, Inc. Amorphous SiC of 97.5% purity consists of 10 × 100 nm\(^2\) laths (stock # 4630js). Nano-β of 97% purity consists of 20 nm particles (stock # 4640ke). Diamond of 95% purity consists of 3 nm particles (stock # 1302jgy). Most SiC samples were dark grey, indicative of excess C or Si, e.g., inclusions of these elements. Nano-diamond is light grey, presumably due to graphite impurities. The α-SiC is pale grey to amber and has little in the way of impurities.

Mid-IR spectra were obtained from \( \sim 450 \) to 4000 cm\(^{-1}\) (2.2 to 25μm) at 2 cm\(^{-1}\) resolution using a liquid-nitrogen cooled HgCdTe detector, a KBr beam splitter and an evacuated Bomem DA 3.02 Fourier transform interferometer. Thin films were created through compression in a diamond anvil cell (DAC) which was used as a sample holder and for the reference spectrum. Efforts were made to cover the entire diamond tip (0.6 mm diameter) with an even layer of sample, but slight irregularities in the thickness were inevitable. Far-IR data were obtained from powder dispersed in petroleum jelly on a polyethylene card from \( \sim 150 \) to 650 cm\(^{-1}\) (\( \sim 15 \) to 67 \( \mu \text{m} \)) using a DTGS\(^2\) detector and mylar beamsplitter. A spectrum

\(^2\)deuterated triglycine sulfate
of nano-diamond (which should be featureless) was subtracted to remove the effect of scattering. For the bulk and nano $\beta + \alpha$ sample, a thin film was made in a DAC and a helium bolometer served as the detector. Far- and mid-IR spectra were scaled to match in the region of overlap and merged. For procedural details see Speck et al. (1999) or Hofmeister et al. (2003).

### 2.2. Laboratory Results

The two nanocrystalline samples have spectra that closely resemble each other, whereas the spectrum of the amorphous sample is most similar to that of bulk $\beta$-SiC (Fig. 1). All samples have three peak complexes centered near 9, 11, and 21$\mu$m. The number and position of the peaks constituting each complex vary, and the relative intensities of the complexes vary among the 4 samples (Table 1). Bulk $\alpha$-SiC shows only the 11 $\mu$m complex. The shoulders in the spectrum shown are due to interference fringes as the overtone-combination peaks in this area are much weaker (e.g. Hofmeister et al. 2000). As it is clear from Fig. 1 that the nano samples have spectra unlike that of $\alpha$-SiC (and $\alpha$-SiC is absent from presolar grains; see § 1.4), the remainder of the discussion concerns the amorphous and $\beta$-SiC samples.

Some of the spectral differences are due to grain size. From Fig. 2 (and Fig. 2 in Hofmeister et al. 2000), as the sample thickens, the LO (longitudinal optic) shoulder increases in intensity relative to the main peak (TO, transverse optic). This occurs because of light leakage (see Hofmeister et al. 2003, for a detailed explanation). The nanocrystalline samples produce spectra close to the expected intrinsic profile (see Spitzer et al. 1959) because their very fine grain sizes aid production of a thin, uniform film that covers the diamond tip. The rounded profiles for $\beta$- and the amorphous SiC are attributed to production of less perfect films from these much larger particle sizes. The difference in relative intensity of the 11 and 9 $\mu$m peaks between the two spectra acquired for amorphous SiC may be due to different film thicknesses and amounts of light leakage as well. However, the relative intensity of this pair varied among the spectrum of the $\beta$-SiC sample, but was consistent for nano $\beta + \alpha$ (Fig. 2 from Hofmeister et al. 2000), suggesting an impurity as the origin.

As observed by Speck & Hofmeister (2004) the relative intensity of the 21 and 11 $\mu$m peaks varied among the samples studied. This observation is supported by the two additional samples studied here, and, intensities of the 21 and 9$\mu$m peaks are roughly correlated (Table 1). A feature similar to the 9$\mu$m peak has been observed in nanocrystals with varying proportions of Si and C by Kimura and colleagues. Carbon films that contain about 30% Si made by evaporation have a peak at 9.5$\mu$m (Kimura & Kaito 2003). From electron diffraction, the structure of the films is nano-diamond and small amounts of $\beta$-SiC are also
present (Kimura & Kaito 2003). Pure diamond structure should not have an IR peak, but impurity bands are well known, such as those due to nitrogen. Apparently, the Si-C stretch in the diamond structure differs from that in the derivative structure of $\beta$-SiC. Higher frequency is consistent with the lattice constant being smaller for diamond than for SiC.

Ion-sputtered carbon films with proportions of 10, 30, and 50% Si similarly contain particles of nano-diamond and IR absorption bands at 9.5 and 21$\mu$m. The 30% film has the most intense 9.5$\mu$m peak, whereas the 50% Si film contains nano-crystals of $\beta$-SiC in addition to the solid-solution nano-diamonds and weak peaks at 11.3 and 12.3$\mu$m (Kimura et al. 2005a).

Nano-particles produced by radio-frequency plasma (Kimura et al. 2005b) absorb at 8.2 (shoulder), 9.2, a doublet at 11.2 and 11.7, and a moderately intense band at 21$\mu$m. The structure is nano-diamond. $\beta$-SiC peaks were rarely seen in the electron diffraction results, suggesting that the IR bands near 11$\mu$m result from short-range order (Kimura et al. 2005b). These authors attribute the 21$\mu$m band to excess carbon which may be present in interstitial sites in the solid-solution nano-diamond particles. The present data corroborate and augment their observations. Bulk $\beta$-SiC, nanocrystalline material, and amorphous nanosamples all behave similarly. In the amorphous sample the structural control is lost so that the sample has places where the $\beta$-SiC structure occurs over nearest neighbors, and places where the nano-diamond structure occurs. These are about in equal proportions. Then there are local sites of excess C giving the 21$\mu$m band. That the 21 and 9$\mu$m peaks are strongest in the amorphous material corroborates assignment of these peaks to excess C in SiC, one of the possibilities proposed by Speck & Hofmeister (2004).

Therefore, the 9$\mu$m peak is indicative of Si-C locally in a diamond structure and the 11$\mu$m of Si–C locally in an SiC polytype. These peaks are found in amorphous SiC (observed here) and nano-diamond crystals (Kimura & Kaito 2003; Kimura et al. 2005a,b). The ratios of these peaks are not correlated, but depend on the Si/C ratio of the material. Either amorphous SiC or nanocrystalline diamond with a high proportion of Si substituting for C are good candidates for the carrier of the 9$\mu$m (see § 3.1) and 21$\mu$m (§ 3.3) features.

2.3. Comparison with astronomical environments

Fig. 3 compares the amorphous SiC spectrum with the observed, double-peaked emission feature seen in the spectrum of Y CVn (original published in Speck et al. 1997). Amorphous SiC provides peaks at the same positions as those observed in the double peaked feature, but not in the same intensity ratio.
The shorter wavelength peak is due to excess carbon forming diamond-like structures in the amorphous or nanocrystalline SiC grains. The relative strengths of the two peaks in the laboratory spectra are controlled by the concentration of excess carbon in the grains. Therefore we can manipulate the composition of the grains to obtain bigger or smaller short wavelength peaks, relative to the longer wavelength Si–C peak. Furthermore, there may be a contribution to the Si–C part of the spectrum from $\beta$-SiC also present in the circumstellar shells, further enhancing the longer wavelength peak relative to the shorter one. Fig. 4 shows the effect of mixing amorphous and crystalline SiC to varying degrees.

Comparing Figures 4 and 5 shows that the double-peaked amorphous SiC spectrum, in combination with $\beta$-SiC can explain the variety of absorption features observed in the spectra of extreme carbon stars (see also § 3.2). The differences in peak positions between the laboratory spectra and the observed astronomical absorption features are due to the effect of self-absorption and grain size, which is discussed in § 4.

3. Spectroscopic studies of carbon stars

3.1. IRAS LRS studies of carbon stars

The spectra of carbon stars change with the evolution of the star. Several studies exist of the evolution of the $\sim11\mu$m feature in carbon star spectra based on IRAS LRS data, but are somewhat contradictory. The majority of carbon stars exhibit the $\sim11\mu$m feature in emission. With the exception of Speck et al. (1997), all attempts to understand the sequence of spectral features fail to include the SiC absorption feature. Here is the summary of the accepted evolutionary trends: Early in the carbon star phase, when the mass-loss rate is low and the shell is optically thin, the $\sim11\mu$m SiC emission feature is strong, narrow and sharp. As the mass loss increases and the shell becomes optically thicker, the SiC emission feature broadens, flattens and weakens. Finally, once the mass-loss rate is extremely high and the shell is extremely optically thick, the SiC feature appears in absorption. Fig. 6 shows spectra from Speck et al. (1997) which demonstrate these trends. Once the AGB phase ends, the dust thins and cools and we begin to see new features that are indicative of the dust in the extreme carbon star phase.

Little-Marenin (1986) found that the majority of $\sim11\mu$m emission features peak at $11.15\mu$m, with only 4% peaking longward of $11.6\mu$m. Baron et al. (1987) found that, as the continuum temperature decreases and the peak-continuum strength of the $\sim11\mu$m emission feature diminishes, the peak position tends to move to longer wavelengths (from $\sim11.3$ to $\sim11.7\mu$m). This trend is demonstrated in Fig. 6. Willem (1988) and Goebel et al. (1995)
found that the stars with high continuum temperatures tended to have the $\sim 11\mu m$ emission feature at $11.7\mu m$, with the $11.3\mu m$ feature arising in the spectra of stars with cool continuum temperatures, an obvious contradiction to the work of Baron et al. (1987). Speck et al. (1997) used a much smaller sample of ground-based UKIRT CGS3 spectra, and found no correlation between the peak position of the $\sim 11\mu m$ feature and the continuum temperature.

Baron et al. (1987) and Goebel et al. (1995) noticed that the decreasing continuum temperature is accompanied by emergence of a second spectral feature at $\sim 9\mu m$. Sloan et al. (1998) found an anti-correlation between the $\sim 9\mu m$ feature and the decreasing continuum temperature, which is opposite to what was observed by both Baron et al. (1987) and Goebel et al. (1995). With such a diverse set of analyses and interpretations of what is essentially the same dataset (except for Speck et al. 1997), no clear correlation can be discerned between changes in the spectral features and evolution of the dust. The differences in interpretation of the IRAS LRS data may stem from differing underestimations of the depth of the molecular (HCN and $C_2H_2$) absorptions, and thus the continuum level (Aoki et al. 1999).

3.2. The SiC absorption feature

The prototype for extreme carbon stars is AFGL 3068 which has an absorption feature at $\sim 11\mu m$, tentatively attributed to absorption by SiC (Jones et al. 1978). Speck et al. (1997) reinvestigated AFGL 3068 and confirmed the absorption features. In addition, Speck et al. (1997) discovered three more extreme carbon stars (IRAS 02408+5458, AFGL 2477 and AFGL 5625) with $\sim 11\mu m$ absorption features, attributable to SiC. Two of these objects (AFGL 2477 and AFGL 5625) exhibited a double peaked absorption feature, with the $\sim 11\mu m$ feature accompanied by a shorter wavelength absorption peak at $\sim 9\mu m$. Speck et al. (1997) attributed this shorter wavelength peak to interstellar silicate absorption along the line of sight, although it is possible that this feature is related to the $\sim 9\mu m$ emission feature that accompanies the $\sim 11\mu m$ emission feature in the spectra of some carbon stars. In all four cases, the $\sim 11\mu m$ absorption feature actually “peaks” at $10.8\mu m$.

The absorption features of AFGL 3068 and IRAS 02408+5458 were revisited by Clément et al. (2003) who showed that these feature, as seen in ISO SWS spectra, were consistent with isolated $\beta$-SiC nanoparticles. However they could not fit the short wavelength side of the $\sim 11\mu m$ absorption feature using SiC alone, which may indicate that the $\sim 9\mu m$ feature absorption is intrinsic to these stars and its strength varies. This will be discussed further is § 6.

The double-peaked absorption features of AFGL 2477 and AFGL 5625 were revisited by
Clément et al. (2005). This work presented new infrared spectra of silicon nitride ($\text{Si}_3\text{N}_4$) and found a correlation between the observed double-peaked feature and the laboratory absorption spectrum. Furthermore, they were able to correlate various weaker longer wavelength absorptions in the astronomical spectra, with those of $\text{Si}_3\text{N}_4$ observed in the laboratory. However, while the match to the longer wavelength features is good, in their laboratory spectra the relative strength of the $\sim 11$ and $\sim 9\mu\text{m}$ features compared to the longer wavelength features indicates that $\text{Si}_3\text{N}_4$ is almost certainly present but cannot be solely responsible for these $\sim 11$ and $\sim 9\mu\text{m}$ absorption features.

Volk et al. (2000) presented the ISO spectra of five extreme carbon stars. They produced radiative transfer models, assuming amorphous carbon dust and including a way to fit the broad $26-30\mu\text{m}$ feature, but without trying to fit the absorption features in the $8-13\mu\text{m}$ range. We have divided the ISO spectra by their model fits, and the resulting spectrum of the $7-13\mu\text{m}$ region is shown in Fig 5, together with the continuum-divided spectra of extreme carbon stars from Speck et al. (1997). It is clear that IRAS 06582+1507 shows the $\sim 11\mu\text{m}$ absorption feature seen in AFGL 3068 and IRAS 02408+5458. The spectrum of IRAS 00210+6221 shows a double/broad feature similar to that of AFGL 5625. IRAS 17534-3030 seems to be intermediate between the two. Given that the extreme carbon star phase is not expected to last more than a few $\times 10^4$ years, it is not surprising that stars which exhibit these features are rare. We now have four stars which exhibit the single $\sim 11\mu\text{m}$ absorption feature, and three which exhibit the broader double feature. It is no longer possible to ignore these absorption features when trying to understand the evolution of dust around carbon-stars.

The $\sim 9\mu\text{m}$ feature/wing appears to correlate with optical depth, appearing strongest when the $\sim 11\mu\text{m}$ feature is in absorption, but also exists when the $\sim 11\mu\text{m}$ feature region weakly emits. This feature may be due to amorphous SiC with excess carbon (see §2), in which case, the formation of such grains occurs when the dust shell is denser, further up the AGB. This makes sense, in that the high density shells may form dust grains so fast that the atoms do not have time to migrate to the most energetically favored position before another atom sticks on. In this way we would expect to form amorphous, rather than crystalline grains. If it is due to nanocrystalline grains, this further supports the hypothesis that grain sizes decrease as mass-loss rates increase. Furthermore, early in the life of a carbon star, the dust forming regions will have more Si than C for dust formation (the majority of the C atoms will be locked into CO molecules). As the star evolves, and more carbon is dredged up from deep within the star, there will eventually be more C atoms than Si atoms and excess C will get trapped in the grains.

The lack of amorphous SiC in meteoritic samples may be due to the relative scarcity
of this form of SiC compared to the crystalline polytypes. A typical AGB star sends dust out into the interstellar medium for a few hundred thousand years, but the extreme carbon star phase is much shorter lived ($< 10^4$ years) and may not occur for all carbon stars (absorption features are rare). Therefore we would expect there to be much more crystalline (mostly $\beta$-SiC) than amorphous SiC grains. Furthermore, there may well be a mixture of amorphous and $\beta$-SiC forming in the circumstellar shells of very evolved (extreme) AGB stars. Alternatively, the meteoritic data may support the attribution of the 9 and 21$\mu$m features to nano-crystalline SiC grains with diamond inclusions. Nanometer-sized SiC grains have been found in the presolar SiC samples (Bernatowicz et al. 2005).

3.3. Carbon-rich post-AGB spectra: the 21$\mu$m feature

Among the C-rich PPNs, approximately half exhibit a feature in their infrared spectra at 21$\mu$m (Omont et al. 1995). Subsequent higher resolution data revised the so-called 21$\mu$m position to 20.1$\mu$m (Volk et al. 1999). PPNs that display this feature are all C-rich and all show evidence of s-process enhancements in their photospheres, indicative of efficient dredge-up during the ascent of AGB (Van Winckel & Reyniers 2000). The 21$\mu$m feature is rarely seen in the spectra of either the PPN precursors, AGB stars, or in their successors, PNs (however, see Volk et al. 2000; Hony et al. 2003). The observed peak positions and profile shapes of the 21$\mu$m feature are remarkably constant (Volk et al. 1999). This enigmatic feature has been widely discussed since its discovery (Kwok, Volk, & Hrivnak 1989) and has been attributed to a variety of both transient molecular and long-lived solid-state species, but most of these species have since been discarded as carriers, except for HACs/PAHs (Justtanont et al. 1996; Volk et al. 1999; Buss et al. 1990; Grishko et al. 2001) and SiC (Speck & Hofmeister 2004). In the case of SiC, it is necessary for the dust grains to be small and contaminated with carbon impurities in order for this feature to appear (Kimura et al. 2005a,b). Furthermore, the cooling and thinning of the dust shell is essential to the emergence of this feature. During the AGB phase, the dust is too warm for this feature to appear, but as the dust cools the $\sim$11$\mu$m feature of SiC is diminished and the 21$\mu$m feature is promoted by the underlying dust-continuum emission. In this case the changing spectrum reflects the change in temperature and optical depth of the dust shell, whereas the spectral features are indicative of the last stage of carbon-rich evolution (the extreme carbon star phase).
4. Self Absorption: the effect of changing grain sizes

Cohen (1984) interpreted the change in the appearance of $\sim 11 \mu m$ feature from sharp and narrow to broad and flat-topped as possibly an effect of self-absorption. This was supported by Speck et al. (1997), who showed that all carbon star spectra in their sample with dust continuum temperatures less than 1200 K needed to have self-absorbed SiC in order to be fitted well. Self-absorption exhibits some interesting characteristics that can be used to diagnose the nature of the dust grains that produce observed spectra.

Figure 7 shows how the absorption profile changes as particle thickness (i.e. grain size) increases. This appears to be a violation of Beer’s Law, in that the absorbance is not simply increasing (for a single wavelength) with thickness of the particles. This departure occurs because the measured intensity depends not only on the amount of light that the sample absorbs, but also on the amount reflected at the surface facing the source. The main peak (the TO mode) becomes saturated in measured spectra when the actual amount of light transmitted at the TO frequency equals the reflectivity. This point is reached at lower thicknesses (grain sizes) for the strong TO mode than for the more weakly absorbing shoulder. Violations of Beer’s law will alter self-absorption in astronomical environments but not emission spectra because the latter are not affected by surface reflections. Therefore, emission spectra of the grains are not so sensitive to the grain size. As long as the grains are still small compared to the wavelength at which they are observed (i.e. grains smaller than $\approx 1 \mu m$ for 10$\mu m$ spectra), the pure emission feature will appear at the same wavelength ($\sim 11.3 \mu m$). However, once the grains are cool enough and the optical depth high enough, self-absorption of the 11.3$\mu m$ feature will begin and the profile of the feature will depend on the relative sizes of the grains.

In computing the effect of Beer’s law violations on self-absorption, we assume that the following holds: (1) the absorbing particles are thicker (larger) than the emitting particles, (2) the light received by the absorbing particles is that of the star = $I_0$, i.e., the inner cloud of emitting particles is rarified enough that it contributes negligible intensity compared to the star, and (3) that outer dust transmits more light that the inner dust emits (i.e. starlight is also transmitted).

Beer’s law states that the wavelength-dependent absorbance $a(\lambda)$ of a given substance is proportional to the mass absorption coefficient $\kappa_{abs}(\lambda)$, and the thickness through which the light has to pass $d$:

$$a(\lambda) = \kappa_{abs}(\lambda)d$$

Deviations from Beer’s law may occur for many reasons. Strictly, Beer’s law applies
to transparent particles (i.e. particles which transmit some light at all wavelengths) and therefore, at high concentrations/opacities may no longer be applicable. Other problems include stray light (McMillan & Hofmeister 1988).

When measuring absorption, we usually measure the transmittivity $T(\lambda)$ of a material and thus obtain the absorptivity $A(\lambda)$:

$$T = \frac{I_{\text{trans}}}{I_0} = 1 - \frac{I_{\text{abs}}}{I_0} = 1 - e^{-a}$$

$$A = \frac{I_{\text{abs}}}{I_0} = e^{-a}$$

The light received from a circumstellar shell $I_{\text{dust}}$ is given by:

$$I_{\text{dust}} = I_{\text{emit}} + I_{\text{trans}}$$

where $I_{\text{emit}}$ is the emission from the inner dust and $I_{\text{trans}}$ is the transmission from the outer dust.

From Kirchhoff’s law, the emissivity is the same as the absorptivity, so that $I_{\text{emit}} = I_{\text{abs}}$

Therefore,

$$\frac{I_{\text{dust}}}{I_0} = f \frac{I_{\text{abs}}}{I_0} + \frac{I_{\text{trans}}}{I_0}$$

$$\frac{I_{\text{dust}}}{I_0} = fe^{-a} + 1 - e^{-a}$$

where the factor $f$ is varied from 0 to 1 as the fraction of light originating from emitting dust increases.

The absorption coefficient will change with grain size $d$, because of the effect of reflections.

$$\frac{I_{\text{dust}}}{I_0} = fe^{-\kappa_{\text{abs,inner}} d_{\text{inner}}} + 1 - e^{-\kappa_{\text{abs,outer}} d_{\text{outer}}}$$

Essentially, Eq. 1 provides the effective transmission of the dust. If Beer’s law is followed (i.e. reflectivity is low and the particles are thin enough to transmit light at all frequencies), then $\kappa_{\text{abs,inner}} = \kappa_{\text{abs,outer}}$ and the spectrum received is no different than the intrinsic absorptions. However, if the absorbing particles are larger, and opaque at some frequencies (i.e.
the TO mode), the spectrum will be altered. We have computed the effect of particle thickness on self-absorption in circumstellar shells, and the resulting spectra are shown in Fig. 7. For $\kappa_{\text{abs,outer}}d_{\text{outer}}$, we used baseline-corrected absorption spectra from the thickest sample of nano $\beta$-SiC shown in Fig. 2, and for $\kappa_{\text{abs,inner}}d_{\text{inner}}$, we similarly used the intermediate sample. The same results would be obtained for the thinnest sample. As the contribution of the emitting particles increases, the contribution of the LO component increases relative to the TO component, and the TO component appears to shift to longer wavelengths.

If the size and absorption coefficients are identical for both the inner and outer regions of the dust shell, then there will be no shift in the spectral features between emission and absorption. However, if the outer grains are larger, there will be a shift in the absorption to shorter wavelengths, shown in Fig. 7.

In terms of what we would expect to see in the sequence of carbon star spectra, the discussion above means that for optically thin dust shells, where we are seeing pure emission, the SiC feature should peak at 11.3\,\mu m and be sharp. As the optical depth goes up, the SiC feature will become self-absorbed, but if the grains in the outer part of the shell are larger than those in the inner zone, the absorption will occur preferentially on the LO side of the feature, diminishing the blue side, which would appear as a shift in the feature to longer wavelengths ($\sim$11.7\,\mu m). As the optical depth gets high enough for the emission feature to be completely absorbed, we no longer see the 11.7\,\mu m feature and the absorption will peak at a shorter wavelength (10.8\,\mu m) than the regular SiC feature at 11.3\,\mu m. This is shown schematically in Fig. 8 (c.f. Fig. 6). This mechanism explains the evolution in the observed SiC absorption feature in extreme carbon stars. Furthermore, it correlates with the evolution of the spectral features as seen by Baron et al. (1987), who showed that as the continuum temperature decreases and the peak-continuum strength of the SiC feature diminishes, the peak position tends to move from $\sim$11.3\,\mu m to $\sim$11.7\,\mu m. This suggests that there is an evolution in the dust grains towards smaller dust grains with higher mass loss.

Two separate studies of presolar SiC suggest that there is an evolution in grain size that corresponds to the evolution of carbon stars. Prombo et al. (1993) found a correlation between grain size and the concentration of $s$-process elements in SiC grains taken from the Murchison meteorites. The Indarch meteorite presolar SiC grains yielded similar results (Jennings et al. 2002). In both cases, the smaller grains have higher relative abundances of $s$-process elements. Since newly-formed $s$-process elements are dredged-up along with carbon from the He-burning shell, they are more abundant in more evolved circumstellar shells than early ones. Therefore, these results suggest that the grains formed around carbon stars decrease in size as the stars evolve and support the observations of the self-absorption effects described above.
Up until now, the generally accepted wisdom has been that low mass-loss rates early in the AGB phase lead to small grains, and increasing mass-loss rates permit the growth of larger grains. In the new scenario, smaller grain sizes with increasing mass loss can be understood in terms of potential nucleation sites. The hardest step in grain formation is the production of seeds onto which minerals can grow. In a low-density gas very few seeds can nucleate, leading to the formation of few grains. However, these few grains can grow large because there are not so many grains competing for the same atoms. Conversely, in a high-density gas, it is easier to form seeds, but so many more nucleate, that there are not enough atoms around for any individual grain to grow large. In this way, high densities lead to very dense dust shells of small grains. This effect may be exacerbated by the earlier outflows moving slower than the later outflows. If the stellar winds that drive the mass loss and send the newly formed grains away from star accelerate with time, then the earlier grains will have more time closer to the star in regions dense enough for grain growth to occur.

Since radiation-pressure coupling should be related to grain composition, and this will vary with the Si/C ratio, we may expect such an effect.

5. Conclusions

The dust shells around carbon stars and their successors, carbon-rich post-AGB stars, evolve along with the star. In early phases, the mass-loss rate is low, and hence the dust shell is optically thin. As these stars evolve, the mass-loss rate increases, and thus the dust shell gets more optically thick, until the star is completely obscured in visible light and very bright in the infrared. During this evolution the relative abundance of silicon to carbon (Si/C) available for dust formation decreases, so that in the early carbon stars there is more Si and C, whereas in the extreme carbon stars there is much more C than Si. Once the AGB phase ends, the existing dust shell spreads out, becoming optically thin and cooler. The combination of increasing density and increasing carbon on the AGB manifests itself in the nature of the dust grains as seen in the spectral sequence for carbon stars.

Early in the carbon star phase, when the mass-loss rate is low and the shell is optically thin, the \( \sim 11\mu m \) SiC emission feature is strong, narrow and sharp. As the mass loss increases and the shell becomes optically thicker, the SiC feature broadens, flattens and weakens. Finally, once the mass-loss rate is extremely high and the shell is extremely optically thick, the SiC feature appears in absorption. The shifts in the peak of the \( \sim 11\mu m \) SiC feature are attributable to a combination of optical depth and grain sizes. The only way to see a shift in the absorption feature to 10.8\( \mu m \) is if the absorbing grains are larger than the emitting grains. Therefore, we have observational evidence to suggest that the grains formed in
circumstellar shell get smaller as the star evolves. Further evidence for this scenario is seen both in post-AGB spectra and in meteoritic studies of presolar grains.

We have presented new mid-IR laboratory spectra for various forms of SiC including amorphous SiC with excess carbon structure. These data corroborate and augment the laboratory work of Kimura & Kaito (2003) and Kimura et al. (2005a,b), indicating that solid solutions of C replacing Si in SiC have the diamond structure on a local scale. This is a good candidate for the carrier of the $\sim 9\mu m$ feature seen in both emission and absorption, and correlated with trends in the $\sim 11\mu m$ feature.

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Fig. 1.— Merged far- and mid-IR spectra of various samples of SiC. Heavy solid line = amorphous SiC. Light solid line = nano-β. Grey solid line = nano-β + α. Dotted line = bulk β. Dashed line = bulk α. Mid-IR segments (λ= 5 to 25µm) are raw data. Far-IR data was scaled to match, but the merging and scaling are equivocal.
Fig. 2.— Dependence of spectra upon thickness. Light lines = nano-$\beta$; Heavy lines = amorphous SiC. Dashed line = thinnest nano-$\beta$ sample; dotted line = thickest nano-$\beta$ sample; thick black line = thinnest amorphous sample; thick grey line = thickest amorphous sample. Raw data are shown.
Fig. 3.— Comparison of double-peaked observed astronomical feature in the continuum-divided spectrum of Y CVn (filled circles) with laboratory spectrum of amorphous SiC (solid line).
Fig. 4.— The effect of mixing amorphous and $\beta$-SiC.
Fig. 5.— Continuum-divided, 7–13\(\mu m\) spectra of extreme carbon stars. Solid lines: ISO SWS spectra divided by model fits from Volk et al. (2000). Dashed line: UKIRT CGS3 spectra divided by best fit blackbody dust continuum from Speck et al. (1997). Spectra are offset in \(y\)-direction for clarity: IRAS 00210+6221 is not offset; AFGL 5625 offset=+0.2; AFGL 2477 offset=+0.4; IRAS 17534-3030 offset=+0.6; IRAS 06582+1507 offset=+0.8; AFGL 3068 offset=+1.0 and IRAS 02408+5458 offset=+1.2.
Fig. 6.— UKIRT CGS3 mid-infrared spectra of carbon stars from Speck et al. (1997). *Top Row:* Solid line = spectrum ($F_{\lambda}$); dashed line = continuum. *Bottom Row:* continuum divided spectra; a,d) Pure SiC emission; b,e) self-absorbed SiC emission; c,f) SiC (self-)absorption. *x-axis* is wavelength in $\mu$m.
Fig. 7.— The effect of thickening dust samples. The fractional factor is $f$ (see Eq. 1), which accounts for more or less light coming from the emitting grains. If the grains are all the same size, the absorption feature is in the same position as the emission feature. If the absorbing grains are larger, then there is an apparent shift in the feature position.
Fig. 8.— Schematic of self-absorption and its effect on the peak position of the $\sim11\mu m$ feature.
Table 1: Spectral parameters* of SiC in various forms.

|                      | bulk δ | amorphous | nano-δ | nano-δ + α | bulk α |
|----------------------|--------|-----------|--------|------------|--------|
| Grain size (nm)      | >1000  | 10 – 100  | 3      | 2 – 5      | —      |
| shoulder (LO; µm)    | 8.4    | 8.4       | —      | —          | 7.66 (sharp) |
| main peak (µm)       | 9.3    | 9.26      | 8.95   | 9.0        | —      |
| shoulder (LO; µm)    | 10.58  | 10.6      | 10.85  | —          | 10.55  |
| Barycenter or main (µm) | 11.30 | 11.43     | —      | 12.14      | 11.85  |
| Main peak or shoulder(µm) | 12.1  | 12.2      | 12.27  | 12.14      | 12.23  |
| peak (µm)            | —      | 16.3      | —      | —          | 16.02 (sharp) |
| shoulder (µm)        | —      | 20        | —      | —          | —      |
| main peak (µm)       | 20.5   | 22        | —      | 21         | —      |
| I₉/I₁₁               | ~0.35  | 0.73      | 0.050  | 0.15       | —      |
| I₂₁/I₁₁              | ~0.1   | ~0.26     | —      | ~0.3†      | —      |

* Peak positions obtained from thinnest samples examined.
† Intensity is very uncertain as the ~ 21µm peak was measured using a dispersion