Optimization of Compaction Quality Control in the Core of Random Fillings within Linear Infrastructures: Application to Metamorphic Slate Fillings

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Abstract: The construction of random fillings from the excavation of medium hardness rocks, with high particle sizes, presents limitations in compaction control. This research applies new control techniques with revised test procedures in the construction of the random fillings core, which constitutes the main part of the embankment, with the bigger volume and provides the geotechnical stability to the infrastructure. The maximum thickness over each of the compacted layers researched that made up the random fillings was 800 mm. As there are many types of rocks, this research is applied to metamorphic slates. Quality control was carried out by applying new research associated with the revision of wheel impression test, topographic settlements, and plate bearing test (PBT). Thus, new test procedures are established, defining efficient thresholds. Comparisons make it possible to choose representative tests, avoiding duplication. The optimization of control reduces inspection times, ensuring quality adapted to the high construction efficiency of diggings. Traditionally, rocks were rejected due to their maximum size, underutilizing the use of high-quality materials. Promoting their utilization implies a better use of resources, and therefore, a higher environmental efficiency. A statistical analysis of the core of 16 slate random fillings was carried out, with a total of 2250 in situ determination of density and moisture content, 75 wheel impression tests, 75 topographic settlement controls, and 75 PBT. The strong associations found between different tests allowed to simplify the quality control.

Keywords: random filling; slate rock; core; wheel impression test; topographic settlement test; plate bearing test

1. Introduction

The Construction Embankment Technical Guide [1] continues to be relevant in landfill monitoring. It recommends compaction control at stone fillings by procedure. It limits the maximum size to 800 mm for the operation of the compaction rollers. The guide recommends procedural control, limiting the application to materials with a maximum size of less than 800 mm. Compaction is defined according to the ratio Q/S compaction intensity, where Q is the volume of the compacted embankment in cubic meters and S is the area swept by the compactor in square meters, the maximum thickness of the compacted layers in meters, the maximum speed of the compactor in kilometers per hour, and the number of roller passes.

Eurocode 7 (EC7) provides a long list of possible limit states and serviceability limit states that should be checked for embankments. It has specific provisions for the supervision of the construction of embankments and the monitoring of embankments during and after construction. It considers that when determining the weight of the embankment
from the specific gravity of the soil, care should be taken to include particles bigger than 20 mm and up to 60 mm in the density tests as they are often not included, although this can have a considerable effect on the specific weight determined. Teijón–López–Zuazo et al. [2] show that in the construction of fillings with stone materials, compaction have limitations that avoid the optimal quality control.

The General Specifications for Roads and Bridges Works PG-3 [3] prescribes macro pits with a minimum surface of 1 m² and 1 m³ of volume. So, it is complex to obtain gradings weighing fractions of different aggregates. For Teijón et al. [4], the nuclear methods for the obtention of density and humidity in situ are not adequate in random fillings for a tested thickness of 300 mm when the layer thicknesses are usually 600 mm. Also, the particle sizes reduce the significance of the test. The density by substitution methods such as sand are not correct, the high hollow introduces errors, limiting its application to 50 mm. For larger sizes the vibration table is recommended.

The modified Proctor test is not a correct reference for the degree of compaction, since it is carried out by substituting material bigger than 20 mm, which in this case is the biggest fraction. Even with these size limitations, the Proctor test is still recommended. Finally, as the plate bearing test (PBT) is a point test, to be representative the diameter of the plate must be 5 times the maximum size, which results in sizes outside the test procedure. The control of topographic settlements needs adequate references, according to Sopeña [5]. The French standard NF P98-736 [6] classifies the compactors according to their load per wheel (CR) as P1, with CR values between 25–40 kN, P2 for CR between 40–60 kN, and P3 for CR > 60 kN. For Fernandez and others [7], test sections are necessary because of the limitations of the compaction control. The tests carried out in this research are shown in Table 1.

Table 1. Random embankments compaction quality control summary.

| Checklist of Tests                  | Limitations                                      | Spanish Procedures               |
|-------------------------------------|--------------------------------------------------|----------------------------------|
| topographic settlements             | no reference values                               | on test sections                 |
| automatic online monitoring         | strong influence on human behavior                | not applied                      |
| pit gradings                        | not practical and unsafe                          | on test sections                 |
| wheel track testing ( UNE 103407)   | minor than 5 mm (works in normal conditions)      | in compaction batches            |
| plate bearing test (UNE 103808)     | diameter of the element 5 times the maximum size  | requires the diameter of the element to be 5 times the maximum size |
| nuclear density gauging (UNE 103900)| particle dimensions                               | not recommended in compaction batches only correlated with other tests |
| modified proctor (UNE 103501)       | replacement 70% fines                             | usually reference to maximum density and optimum moisture |
| sand method (UNE 103501)            | maximum size < 50 mm                              | in compaction batches            |

Nowadays, the quality control methods for earthworks are highly developed through several research projects that made it possible to use inadequate quality materials. The current specifications are sufficient for the control of this type of material. However, the specifications for the control of the laying of stone materials (rockfills and random fillings) are underdeveloped.

The granulometric analysis of stone formations by inspection pits can be carried out by weighing the fractions, although it is of limited operability. Average density control has the limitations of nuclear methods for density and moisture determinations. The limitations of the test also affect the layer thickness tested. A more accurate method for compaction control in rockfills is the measurement of settlement by topographic procedures, although practical reference values need to be defined. The values required for the wheel impression test do not impose any limitations on the usual compaction conditions.
The procedure for testing the wheel impression test on fillings involves the measuring points being measured by means of a tape measure attached to two survey markers. The measuring element on which the survey marker is placed consists of a set of welded metal frames which, because of their interlocking arrangement, is usually known as ‘H’. The measurement is carried out by placing the metal device on each measuring point, before and after the loaded truck has passed. The wheel impression value is calculated as the arithmetic mean of the 10 points ($\delta_m$). This value is called the compaction degree index.

The main reasons proposed are to define a new method of compaction control, applying only representative tests and thresholds, and the revision of procedures in the wheel-tracking test and in the topographic settlement, avoiding limitations. Among the different types of rock, research is focused on the family of slate rocks. Fernandez et al. [7] consider that rocks with a single compressive strength below 25 MPa produce random fillings of sufficient quality, performing test sections with excellent results. Rahman et al. [8] relate the compactor placed on the vibratory rollers with the calculation of the instantaneous density, finishing the compaction when the dynamic module is reached. This method can be used to locate soft spots by means of a global positioning system (GPS). Oteo [9] considers granulometry and density as the main parameters to be defined for use in the formation of fillings. Lim [10] says that Korean road specifications include a 30 cm layer thickness that avoids the use of rocks. There are also no specifications for quality control with stone materials. He proposes obtaining the density on site by the “water replacement method” within the inspection pit. For Sakaia et al. [11], the revision of the Road Embankment Earthquake Manual does not sufficiently consider the influence on the mechanical behavior of soil compaction. Triaxial tests have associated the highest load deviation with the compaction degree. One-dimensional consolidation tests allowed a linear adjustment of the compression curve. The highest dry density corresponds to the lowest compressibility, although overconsolidation can produce the collapse of the structure.

The compaction procedure for random fillings, in accordance with PG-3 [3], should define the optimum moisture content, the number of passes, the maximum layer thickness, and the machinery to be used for earthworks. Kyung–Tae et al. [12] investigate the execution of a rock embankment built by dynamic compaction performing PBT. Due to dynamic compaction, an increase in pressure can develop in the foundation. A hyperbolic model associated with the construction method was adjusted to the seat. The estimated results were compared to the settlements and the results of PBT.

Oteo [9] considers that geophysical prospecting techniques, in addition to the plastic sheet substitution method, are suitable for the control of random fills. Nuclear methods present problems, such as the penetration of the emitting rod between rock fragments. It can be measured by backscattering, that is, by direct emission from the surface, although the results are not reliable because they correspond to the most compacted area. In the study of space exploration, research was carried out to estimate soil density by means of drone drilling. Similar methods can be applied to quality control in compaction. Iai et al. [13] fit a model by obtaining the density of the raked soil by raking force. The application of the method allows the support of the drone on the moon or Mars in addition to the Earth. Scale models were made with JSC-1a (artificial lunar regolite), obtaining relationships between the density of the soil or lunar regolite, the ripple force, and the spacing and number of scarifiers. The instrumentation allows a high-resolution mapping of the density of the raked site, providing an in situ calibration of the ground by remote control from the Earth. For Wu and Wang [14], the effect of the time between the layers on field compaction must be considered in the construction of filler. For longer surface exposures, moisture tends to evaporate, and test results change. With the Clegg soil impact test hammer, compacted Xiangshan sand was practical for dry density measurement. The force of compacted sand and compaction effort correlated well with the soil impact test hammer. The main factors influencing the compacted Xiangshan sand were moisture and degree of compaction. Lower compaction effort results in lower soil strength as moisture content increases. The stability of the embankments depends on the quality of the compaction of
the fill. Nondestructive testing techniques have more advantages than that of conventional field density tests. Therefore, the use of nondestructive testing techniques in fill monitoring seems interesting in geotechnical applications. Using the Clegg impact tester, impact (Iv) values varying in compaction effort, moisture content, and density were observed in the laboratory. The variations of Iv with moisture are equal to the moisture-density ratio. The Iv has a strong relationship, for each compaction effort, with the moisture-density ratio. With a simple moisture test, the dry density can be predicted using the Iv values. This allows efficient quality control compaction.

Cacciola et al. [15] performed a geo-analytical investigation. The use of frequent surveys adds both costs and delays to earthwork projects. With continuous compaction control and intelligent compaction systems, they provide a real-time monitoring. This is the Real-Time Kinematic Global Positioning System. This process can be used with great benefit by ensuring the quality of the compacted soil. In addition, Liu et al. [16] proposed an innovative process for quality control in earth rock engineering. The compaction monitoring technology integrated into the rollers was combined with real-time global positioning kinematics, adopting the value of compaction as real-time monitoring. The compaction value has decreased with the speed of the rollers, increased with the decrease of the layer thickness, and increased with the increase of the dry density. Thus, the compaction value has a relation with the quality control of the compaction. Therefore, the compaction value is similar to the compaction meter value used by the geodynamic engine drive power. Therefore, it can serve as a real-time characterization, identifying the quality control of the compaction. Regression models were used with compaction value, moisture, and gradation as independent variables. Rapid and continuous evaluations of the compaction quality control prevent quality defects and improve the quality of the embankment construction, traditionally controlled through compaction thickness, vibration condition, compaction passes, and roller speed. These are limited point samples to represent the construction quality of the entire work area can be unreliable, with delays in rectification of problems at the paving site.

Sawangsuriya et al. [17] commented that quality control in road compaction in Thailand is based on in-situ density measurements using the sand method. Quality monitoring is basically carried out through the sand cone test, UNE 103503 [18]. This is a simple test, although it generally requires a long testing time and is a destructive procedure. A laboratory machine provides a rapid impedance-based measurement of density and moisture in electrical spectroscopy. They investigated the density and moisture results with other tests such as nuclear methods, PBT, sand method, etc. Anjan Kumar et al. [19] proposed an alternative method by setting target values according to soil characteristics, trying to avoid test sections. By measurement of rollers and nondestructive tests, different soils were analyzed. The in-situ tests carried out were the dynamic penetrometer, the light deflectometer and the density measurement by radioactive isotopes. With the use of the intelligent compaction, they established correlations between the values of the in-situ ensembles and the measurements of the rollers, quantifying the improvement of the material at the passing of the compacting rollers.

Nazarian et al. [20] evaluate modules as a function of moisture from the portable seismic analyzer. While all sections tested with the nuclear density meter exceeded the traditional 95% maximum dry density acceptance limit of the modified Proctor test, the modules estimated with ultrasonic surface wave technologies are higher than the moisture-dependent adjusted module. Mansour and Aly [21] adopted the Modflow program for modelling groundwater flow conditions. Using a genetic algorithm, they achieve optimization to minimize the number of wells. Road construction requires high water consumption for compaction. Thus, groundwater optimization contributes to future drainage projects and can be applied in construction excavations to obtain satisfactory quality control.
The Portancimeter, developed at the Laboratoire Central des Ponts et Chaussées, consists of the passing of a one meter diameter wheel of 400 kg with an eccentric introducing a vibration of 35 Hz, the reaction being a suspended mass of 600 kg. The modulus of stiffness is obtained with an accelerometer on the wheel axle which measures the experienced settlement.

Similar techniques are used in the compactometer, using intelligent compaction rollers, IC rollers. IC rollers have an accelerometer in the bracket and a gauge on the dashboard, visible to the operator. The ratio between the amplitude of the acceleration of the first harmonic of the wave and the amplitude of the fundamental frequency is evaluated at time intervals between 5 and 30 s. The accelerometer changes its shape with increasing number of passes. With the first pass, the signal is almost sinusoidal; a distortion is produced which increases with the number of passes. The test depth can exceed 150 cm. The compactometer measurement is correlated with the density instantaneously. Once the minimum value of the required dynamic modulus is obtained, the operator stops making additional roller passes over the compacting layer. The method can be used in checks to locate soft spots, and the information can be completed with a global positioning system (GPS).

The statistical analysis of the main compaction trials was carried out, obtaining correlations. Due to the large size of the explanations, the study was particularized to the core zone, with a maximum layer thickness of 800 mm. The tests carried out were applied the revised procedures of the topographic settlement and the wheel impression test [2].

2. Material and Methods

2.1. Material

This research was done on the A-66 Spanish highway, Cáceres, Aldea del Cano section, with 21 slate random fillings for a 3,000,000 m³ rock digging approximately. Table 2 provides examples of the tests that were conducted on the slate alluvial material during excavation, with the last row showing average values.

Table 2. Examples of physical parameters for slate alluvial material identification.

| Ref.    | # 100 (mm) | # 20 (mm) | # 2 (mm) | #0.40 (mm) | #0.075 (mm) | Liquid Limit (LL) | Plastic Limit (PL) | Plasticity Index (PI) | Membership USGS index | Dry Density (g/cm³) | Humidity (%) | CBR |
|---------|------------|-----------|----------|------------|-------------|-------------------|---------------------|----------------------|----------------------|---------------------|--------------|-----|
| CC-017  | 100.0      | 56.0      | 29.0     | 20.0       | 14.5        | 29.5              | 21.4                | 8.1                  | 0.900                | 2.14                | 6.7          | 25.8 |
| CC-014  | 100.0      | 54.0      | 22.0     | 16.0       | 13.3        | 31.8              | 24.1                | 7.6                  | 0.900                | 2.14                | 6.8          | 14.0 |
| CC-015  | 100.0      | 40.0      | 17.0     | 14.0       | 11.5        | 31.9              | 19.4                | 12.5                 | 0.900                | 2.05                | 8.8          | 9.3  |
| I-09030/04 | 100.0  | 66.0      | 41.0     | 28.0       | 20.6        | 35.0              | 24.3                | 10.7                 | 0.600                | 2.06                | 5.3          | 21.1 |
| CC-011  | 100.0      | 89.0      | 53.0     | 46.0       | 38.4        | 30.3              | 23.4                | 6.9                  | 0.800                | 2.10                | 7.5          | 6.6  |
| CC-027  | 100.0      | 72.0      | 47.0     | 35.0       | 26.0        | 28.0              | 21.7                | 6.4                  | 0.800                | 2.10                | 10.0         | 25.8 |
| Averages| 100.0      | 64.0      | 35.7     | 26.3       | 21.1        | 31.9              | 22.3                | 9.9                  | 0.817                | 2.05                | 8.9          | 15.5 |

The analyzed soils come from the alteration of the slates, with a high percentage of coarse fraction, 64% by the 20mm sieve and 21% fine content, and low plasticity by the Atterberg limits. High values of the CBR index were obtained, around 15. The membership index of USGS for each random filling part is presented as a numeric index ranging from 0 to 1, where the higher the index number the more fully a soil is a member of the set, and thus, the greater the degree of limitation or suitability for a specific use.

For the expected engineering behavior of the rocks, field boreholes were carried out before the excavations. The codification has attempted to unify the description of rocks with its origins in geology. The tests to identify the main geomechanical parameters done on samples of metamorphic rocks, which belong to the slate family, are shown in Table 3. The description of mass rocks was covered on weathering, description of discontinuities, and fracture state logging. Since there, the boreholes are methods of identifying discontinuities data in the field, as well as method of presenting data of this type of rocks. Some areas are less important, which presents big difficulties, so such a description of slates’ mixed colors or the stratigraphic names were omitted in the research.
Table 3. Geomechanical evaluation of rock mass (RMR determination).

| Depth (m)  | Lithology | Weathering Grade | UCS (kp/cm²) | RQD (%) | Diapause Spacing (mm) | Water Freatic | RMR |
|------------|-----------|------------------|--------------|---------|-----------------------|---------------|-----|
| 3.40–7.10  | slate     | IV–V             | 7.40         | 90.00   | 0.33                  | almost dry    | 53  |
| 7.10–14.60 | slate     | III–IV           | 100.90       | 85.00   | 0.33                  | almost dry    | 55  |
| 14.60–16.00| slate     | III              | 194.00       | 90.00   | 0.33                  | almost dry    | 55  |
| 2.20–4.30  | shale     | III–IV           | 30.00        | 0.00    | 0.30                  | slightly wet  | 22  |
| 4.30–9.00  | shale     | III–IV           | 122.00       | 21.00   | 0.13                  | slightly wet  | 38  |
| 9.00–10.00 | shale     | III–IV           | 30.00        | 0.00    | 0.03                  | slightly wet  | 22  |
| 3.50–5.80  | slate     | IV–V             | 104.70       | 10.00   | 0.03                  | almost dry    | 34  |
| 5.80–7.80  | slate     | III–IV           | 104.70       | 50.00   | 0.40                  | almost dry    | 46  |
| 7.80–8.55  | grauwacke | III              | 44.60        | 50.00   | 0.40                  | almost dry    | 46  |

where:
- UCS: unconfined compressive strength [kp/cm²].
- RQD: rock quality designation—a quality index proposed by Deere. It is the relation of the percentages between the sum of the recovered pieces from the borehole with length higher than 10 cm and the total length drilled in the maneuver. This length depends on the compactness of the ground, and in this investigation, it was basically between 1.5 and 3.0 m.
- RMR: rock mass rating—quality index of the rock, which was calculated based on other parameters such as unconfined compressive strength (UCS), the RQD evaluated previously, the spacing, condition and orientation of the discontinuities, and, lastly, the presence of water.

So, the description of rocks was done with the best tool possible, that are the unaltered samples from a borehole. The nomenclature of codification and description references to the latest codes and standards (EN ISO 14688, EN ISO 14689). Thus, 4 samples were classified by their resistance as very weak rock, $1.0 \leq \text{UCS} \leq 5.0$, and other 3 values as weak rock, with resistances between $5.0 \leq \text{UCS} \leq 12.5$ [MPa]. Finally, one sample was classified as extremely weak, $0.6 \leq \text{UCS} \leq 1.0$ and another as moderately weak rock, $12.5 \leq \text{UCS} \leq 25.0$. Figure 1 was plotted with geological cross-section graph to understand easily.

The weathering degree was defined according to the ENV 1997-3:1999 standard, with all samples being classified in grades III and IV. Grade III corresponds to moderately weathered rocks, in which less than half of the rock material decomposed or disintegrated into the soil. At this grade, fresh or discolored slate rock is preserved as a rock core. Grade IV, on the other hand, is reserved for rocks of the highly weathered shale family. They belong to the rocks that decomposed in soil into more than half of the rock material. Fresh or discolored slate rock was observed in a discontinuous manner.

In general, they are rocks and soils from the alteration of slate, with a low-medium plasticity. According to the USCS classification, they mainly belong to the GC group, classified as coarse-grained soils wrapped in a clay matrix. There are large sizes of the mother rock, with a sift length through the 20 mm sieve of only 74%, and at the same time an important percentage of fines, with an average pass through the #0.08 mm sieve of 21%. As there were several degrees of weathering of the parent rock, a significant number of samples were classified within the group of high plasticity (MH) silts. With these values, the digging materials corresponding to investigated slate rock masses are valid for use in foundation fill, cores, and transition zones in random fillings.
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2.2. Methods

The field and laboratory works were developed to elaborate new test procedures for a proposed compaction control in rocks. In this research, the modified compaction control tests according to Teijón–López–Zuazo et al. [2] were used, which modify the test...
procedures in the wheel-tracking test and in the topographic settlements. It was proposed as a measurement criterion the settlement between the penultimate and last pass of the compacting roller, which in case of random filling core, should be less than 5mm. The measuring system was changed from being undefined to having levelling picks distributed in 2 rows of 5 points spaced 10 m.

The study was applied to the core random fillings with slate rocks. To facilitate interpretation, the core also includes foundations and shoulders, as shown Figure 2.

![Schematic diagram of random filling parts.](Figure 2)

All the tests that were used in the experiment are shown in Table 4.

Table 4. Compaction tests used in research.

| laboratory | field |
|------------|-------|
| 2250 nuclear methods | 75 wheel impression |
| 425 modified Proctor | 75 topographic settlements |
| UNE 103900 [22] | UNE 103407 [24] |
| UNE 103501 [23] | PG-3 [3] |
| | 75 PBT |
| | UNE 103808 [25] |

The wheel tracking test is measured with a “H” dispositive, Figure 3a. The truck should be conducted through topographic leveling pegs, as Figure 3b.

The results of the revised test (h) are the different measurements before and after the passing of the truck in millimeters, Figure 4. The pegs reduce the possibility of extreme erroneous observations and the chances of any potential errors.

The revised topographical settlement procedure was also used. The results are the settlements in millimeters between the penultimate and last roller pass. As shown in the Figure 5, the first pass has easily exceeded such settlement threshold (one per cent of the thickness layer). Therefore, this control method and its limitations were thoroughly revised in the research.
Figure 3. (a) Measurement structure, “H” (b) Passing of twin wheels over peg.

Figure 4. Topographic settlement measured after roll pass.

Figure 5. Topographic settlement–roller passes. 800 mm section random filling.
The compaction degree proposed is associated with a modified Proctor compaction energy level. All the tests were performed under the same moisture conditions to prevent soil stiffness increases and noticeable dry density decreases in the plate bearing test as a result of decreases in water content to below optimum.

The criteria suggested to quality control in core of random embankments were grouped in Table 5.

Table 5. Specifications suggested for core random fills in optimization of quality control.

| Density of Compaction (%) | h (mm) | s (mm) | Ev₁ (MPa) | Ev₂ (MPa) | k (Ev₂/Ev₁) |
|---------------------------|-------|-------|--------|--------|----------|
| 95.0                      | ≤4.0  | ≤4.0  | ≥30.0  | —      | <3.0     |
| — not required            |       |       |        |        |          |

In the statistical analysis, a minimum value of the determination coefficient of 0.70 was chosen to define a correlation between the variables. As a result, 2-variable linear models are better suited than multivariable models. There is no difference between dependent and independent variables.

The specific schematic diagram of compaction tests relationships is shown in Figure 6.

3. Results

Linear correlations between 225 lots were evaluated. There was no relation between density–topographic settlement test, wheel-tracking–topographic settlement test, or first–second modulus PBT (φ 600 mm). The variables were entered into the SPSS Statistics calculation program. An analysis of variance ANOVA shows the sums of squares and the degrees of freedom associated with each: is significant at p < 0.05. A multitude of nonlinear models were analyzed, although finally all the adjustments were linear because no curve was found that has significantly improved the adjustments.

3.1. Relation Wheel-Tracking—Topographic Settlement Tests

As shown in Figure 7, there is a correlation between the wheel-tracking and the topographic settlement tests. The association is directly proportional, with higher values of the wheel rut corresponding to higher topographic settlements.
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![Figure 7. Scatterplot wheel-tracking (h)—topographic settlement (s).](image)

The high value of the Pearson correlation coefficient $\rho = 0.843$ (R in table) shows a strong relationship between the wheel-tracking and the topographic settlement tests, as detailed in Table 6. The coefficient of determination $R^2 = 0.710$ means a variance percentage of 71.0%. The standard error is 0.1475 mm.

Table 6. Determination coefficients of wheel-tracking and topographic settlement tests.

| Summary Model | R      | $R^2$  | $R^2$ Fit | Standard Error |
|---------------|--------|--------|-----------|----------------|
|               | 0.843  | 0.710  | 0.637     | 0.1475         |

*Predictors: constant, h (mm).

As shown in Table 7, Levene test is significant with a value of $F = 9.786$ (Hartley’s $F$). Consequently, the homoscedasticity criterion is not met. The variances are different. The variables, therefore, are related.

Table 7. Variance analysis wheel impression and topographic settlement tests.

| Model            | Sum of Squares | Degrees of Freedom | Quadratic Average | F     | Sig.   |
|------------------|----------------|--------------------|-------------------|-------|--------|
| regression       | 0.213          | 1                  | 0.213             | 9.786 | 0.035  |
| sampling error   | 0.087          | 4                  | 0.022             |       |        |
| total            | 0.3            | 5                  |                   |       |        |

*dependent variable: s (mm) *predictors: (constant), h (mm.)

Table 8 shows high $t$-values (Student’s $t$ test) of 11.237 and 3.128, both significant. The wheel-tracking test permits an accurate prediction of the topographic settlement values, which allows for the substitution of the compaction control procedure and vice versa.
Table 8. Linear regression coefficients in wheel-tracking and topographic settlement tests.

| Model      | Nonstandard Coefficients | Standard Coefficients | t   | Sig. |
|------------|--------------------------|-----------------------|-----|------|
| (constant) | 2.446                    | 0.218                 | 11.237 | 0.000 |
| h (mm)     | 0.257                    | 0.082                 | 0.843 | 3.128 | 0.035 |

* dependent variable: s (mm).

According to the coefficients, the linear fit equation for the topographic settlement and the wheel-tracking tests is:

\[ s = 2.446 + 0.257 \, h \quad R^2 = 0.710 \quad (1) \]

The function domain uses the intervals of \([2.5 \leq s \leq 3.5]\) and \([1.5 \leq h \leq 4.0]\).

3.2. Relation Wheel-Tracking Test—First PBT Modulus

As shown in Figure 8, there is a high correlation between the wheel-tracking test and the first PBT modulus (\(\phi\) 600 mm), with inverse proportionality. In this case, high values for the wheel-tracking test correspond to low values for the first PBT modulus.

![Figure 8. Scatterplot for wheel-tracking test and first modulus PBT (\(\phi\) 600 mm).](image)

Table 9 shows a high Pearson correlation coefficient value, \(\rho = 0.990\), which is associated with low dispersion. The coefficient of determination \(R^2 = 0.980\) yields a variance of 98%. The standard error is only 4.1934 MPa.

Table 9. Determination coefficients for wheel-tracking test and first PBT modulus.

| Summary Model | R     | R^2  | R^2 Adjusted | Standard Error |
|---------------|-------|------|--------------|----------------|
|               | 0.990 | 0.980| 0.975        | 4.1934         |

* Predictors: constant, h (mm.)

Table 10 shows the ANOVA results. Levene’s test proved significant sig = 0.000 with a value of F = 199.826. Therefore, the null hypothesis of homoscedasticity is rejected, and variances are significantly different.
Table 10. Variance analysis wheel impression test and first PBT modulus.

| Model          | Sum of Squares | Degrees of Freedom | Quadratic Average | F      | Sig. |
|----------------|----------------|--------------------|-------------------|--------|------|
| regression     | 3513.855       | 1                  | 3513.855          | 199.826| 0.000|
| sampling error | 70.338         | 4                  | 17.585            |        |      |
| total          | 3584.1932      | 5                  |                   |        |      |

a dependent variable: Ev₁ (MPa) b predictors: (constant), h (mm)

The t-test in Table 11 offers high values, 32.576 and −14.136, both significant (sig = 0).

Table 11. Linear regression coefficients wheel-tracking test—first PBT modulus.

| Model          | Nonstandard Coefficients | Standard Coefficients | t     | Sig. |
|----------------|--------------------------|-----------------------|-------|------|
| (constant)     | 129.468                  | 3.974                 | 32.576| 0.000|
| h (mm)         | −26.291                  | 1.904                 | −14.136| 0.000|

a dependent variable: Ev₁ (MPa.)

Moreover, the wheel impression test predicts the first vertical modulus of the plate bearing test. Besides the linear regression coefficients, the fit between the wheel impression test and the first modulus of the PBT (ϕ 600 mm) is:

\[ Ev₁ = 129.468 - 26.921 h \quad R^2 = 0.980 \quad (2) \]

The domain of the function between the intervals is \([20 \leq Ev₁ \leq 110]\) and \([0.5 \leq h \leq 4.5]\).

3.3. Relation Topographic Settlement Test—First PBT Modulus

As shown in Figure 9, there is a strong correlation between the topographic settlement test and the first modulus plate bearing test (ϕ 600 mm).

Figure 9. Scatterplot for topographic settlement test—first PBT modulus (ϕ 600 mm).
Table 12 shows a high Pearson correlation coefficient value, $\rho = 0.962$, and a low standard error of $Se = 7.1343$ MPa. The coefficient of determination validates a variance of 92.5%. All the parameters suggest a high correlation between both variables.

**Table 12.** Determination coefficients topographic settlement test—first PBT modulus.

| Summary Model | $R$ | $R^2$ | $R^2$ Adjusted | Standard Error |
|---------------|-----|-------|----------------|----------------|
|               | 0.962 $^a$ | 0.925 | 0.9 | 7.1343 |

$^a$ Predictors: constant, $s$ (mm.)

ANOVA parameters are in Table 13. Levene’s test is significant, $F = 36.847$, $sig = 0.009$. The homoscedasticity criterion is not clearly met. Since the variables are strongly related, variances are significantly different.

**Table 13.** Analysis of variance for topographic settlement and first PBT modulus.

| ANOVA $^a$ |
|-------------|
| Model       | Sum of Squares | Degrees of Freedom | Quadratic Average | $F$ | Sig. |
| regression  | 1875.433       | 1                  | 1875.433          | 36.847 | 0.009 $^b$ |
| sampling error | 152.695       | 3                  | 50.898            |      |      |
| Total       | 2028.128       | 4                  |                  |      |      |

$^a$ dependent variable: $Ev_1$ (mm); $^b$ predictors: (constant), $s$ (mm).

Table 14 shows high $t$-values of 9.884 and $-6.070$, which are both significant. The topographic settlement test predicts the first PBT modulus ($\phi 600$ mm).

**Table 14.** Linear regression coefficients for topographic settlement and first PBT modulus.

| Coefficients $^a$ |
|-------------------|
| Model             | Non-Standard Coefficients | Standard Coefficients | $t$ | Sig. |
|                   | B | Standard Error | Beta |     |     |
| (constant)        | 169.243 | 17.124 |       | 9.884 | 0.002 |
| $h$ (mm)          | -24.549 | 4.044 | -0.962 | -6.070 | 0.009 |

$^a$ dependent variable: $Ev_1$ (MPa).

According to the linear regression coefficients, the adjustment line is:

$$Ev_1 = 169.243 - 24.549 \, s \quad R^2 = 0.925 \quad (3)$$

The domain of the function uses the [20 $\leq$ $Ev_1$ $\leq$ 100] and [3.0 $\leq$ $s$ $\leq$ 6.0] intervals.

### 3.4. Relation Topographic Settlement Test—Second PBT Modulus

As shown in Figure 10, there is a high correlation between topographic settlement and first PBT modulus. The distribution is inversely proportional to the lower settlement values corresponding to the higher values of the second PBT modulus ($\phi 600$ mm).
Figure 10. Scatterplot for topographic settlement test and second PBT modulus.

Table 15 illustrates a high Pearson correlation coefficient, $\rho = 0.995$. There is a low standard error $Se = 4.5260$ MPa and a high coefficient of determination $R^2 = 0.990$. There is low dispersion.

### Table 15. Determination coefficients for topographic settlement test and second PBT modulus.

| Summary Model | $R$ | $R^2$ | $R^2$ Adjusted | Standard Error |
|---------------|-----|-------|----------------|----------------|
|               | 0.995 a | 0.990 | 0.985 | 4.5260 |

a Predictors: constant, $s$ (mm).

The ANOVA analysis parameters are shown in Table 16. Levene’s test is significant, $\text{sig} = 0.005$ with $F = 19.251$, and therefore, the assumption of homoscedasticity criterion is not met, since variances are different and have a dependency relationship.

### Table 16. Variance analysis for topographic settlement test and second PBT modulus.

| ANOVA a | Model | Sum of Squares | Degrees of Freedom | Quadratic Average | F | Sig. |
|---------|-------|----------------|--------------------|-------------------|---|------|
|         | regression | 3951.860 | 1 | 3951.860 | 19.251 | 0.005 b |
|         | sampling error | 40.970 | 2 | 20.845 |
|         | total | 3992.830 | 3 |

a dependent variable: $Ev_2$ (mm); b predictors: (constant), $s$ (mm.)

Student’s $t$ test values are significant. As shown in Table 17, there is a significant contribution of the topographic settlement in the second modulus plate bearing test ($\phi$ 600 mm).
Table 17. Linear regression coefficients for topographic settlement and second PBT modulus.

| Model | Nonstandard Coefficients | Standard Coefficients | t | Sig. |
|-------|---------------------------|------------------------|---|------|
| (constant) | 403.329 | 15.493 | 26.420 | 0.001 |
| s (mm) | 48.108 | 3.464 | −0.995 | −13.889 | 0.005 |

* dependent variable: $E_{v2}$ (MPa).

The expression of the adjustment line is:

$$E_{v2} = 403.329 - 48.108 \cdot s \quad R^2 = 0.985 \quad (4)$$

The domain of the function has values between $[140 \leq E_{v2} \leq 240]$ and $[3.5 \leq s \leq 6.0]$.

3.5. Significance Matrix

For better understanding, a matrix of significance is shown in Table 18 with the results obtained. If no relationship was obtained, the numerical value is replaced by ns (nonsignificant). Some elements of the matrix are not considered because they are easily deduced.

Table 18. Slate core random fill significance matrix.

| Determination Coefficients ($R^2$) | d (g/cm$^3$) | h (mm) | s (mm) | $E_{v1}$ (MPa) | $E_{v2}$ (MPa) | k ($E_{v2}/E_{v1}$) |
|-----------------------------------|-------------|--------|--------|----------------|----------------|-------------------|
| d (g/cm$^3$)                     | ---         | ns     | ---    | ns             | ---            | ---               |
| h (mm)                           | ns          | ---    | ---    | ns             | ---            | ---               |
| s (mm)                           | ns          | 0.710  | ---    | 0.874          | 0.925          | ---               |
| $E_{v1}$ (MPa)                   | ns          | 0.874  | 0.925  | ---            | ---            | ---               |
| $E_{v2}$ (MPa)                   | (*)         | ns     | 0.990  | ns             | ---            | ---               |
| k ($E_{v2}/E_{v1}$)              | (*)         | ns     | (*)    | (*)            | Ns             | ---               |

ns: nonsignificant; (*) obvious relationships.

The values of the student $t$ test were grouped in Table 19.

Table 19. Slate core random fill significance matrix.

| Student $t$ Test ($t$) | d (g/cm$^3$) | h (mm) | s (mm) | $E_{v1}$ (MPa) | $E_{v2}$ (MPa) | k |
|------------------------|-------------|--------|--------|----------------|----------------|---|
| d (g/cm$^3$)           | ---         | ns     | ---    | ns             | ---            | ---|
| h (mm)                 | ns          | ---    | ---    | ns             | ---            | ---|
| s (mm)                 | ns          | 3.128  | ---    | −14.136        | −6.070         | ---|
| $E_{v1}$ (MPa)         | ns          | −14.136| −6.070 | ---            | ---            | ---|
| $E_{v2}$ (MPa)         | (*)         | ns     | −13.890| ns             | ---            | ---|
| K                      | (*)         | ns     | (*)    | (*)            | ns             | ---|

ns: nonsignificant; (*) obvious relationships.

3.6. Discussion

The wheel impression test has a reduced test length in the batch on a single margin and a low precision due to levelling in soils. With the alternative method, levelling pikes were defined, a higher number of determinations on both ruts and over a larger length. This revision was implemented satisfactorily. In the wheel impression test, a high correlation with other compaction control tests was obtained, which made it possible to replace it as redundant. In addition, the low sensitivity of the test made it possible to further restrict the acceptance threshold to 4 mm. The classical procedure by topographic settlement control is
insufficient. A new origin was defined in the penultimate roller pass and the acceptance measure was quantified satisfactorily according to the test section. It is considered essential to limit the execution of big pits due to the operational complexity associated with large sizes. Also, it is necessary to consider the execution of plate load tests on 600 mm plate in random fillings.

The advantages of the revised procedure, compared to the French standard SNV 670 365 “Contrôle du Compactage par essieu de 10 t” are:

- Obtaining the compaction degree index in a length five times longer than the initial one, with twice as many measurements for the same section of all-in-one backfill;
- Reduction of levelling errors by having a fixed point on the metal levelling spike and not on the ground, guaranteeing millimetric precision;
- Increased performance by reducing test times, with the first measurement being made on the picks without the need to move the heavy metal support used in the measurement;
- The possible dynamic effects of acceleration/braking of the truck are minimized by increasing the distance travelled and increasing the time taken for the truck to establish a constant speed when passing over the cutting tools;
- With two measurements per profile, a more complete check of the all-one fill section is made than with a single point. By measuring in two parallel and independent tracks, any deficiencies in one track are corrected. In addition, second-order effects such as the weight of the driver or the fuel tank are no longer considered in the test;

The in-situ density did not correlate with any other variable. Alternatively, with the first PBT modulus (ϕ 600 mm), the wheel-tracking and topographic settlement tests proved to have a strong relationship. A revised control method was designed for the in-situ density test and the PBT.

There is a strong correlation between the revised topographic settlement test and the plate bearing test (ϕ 600 mm) so the PBT can be easily replaced. With significant improvements in both the topographic settlement test and the wheel impression test, the PBT is associated with both, so the PBT (ϕ 600 mm) can replace these tests in quality control.

The nuclear methods have a low efficiency, limited by a maximum test thickness of 300 mm and the high variability of the materials. Therefore, the PBT (ϕ 600 mm) is proposed as the most representative test to define the degree of compaction in the new control method. As this test is strongly associated with surface moisture, it should be carried out in the same area of validity as the optimum moisture obtained in the modified Proctor.

As factors that can potentially produce errors in the results, the Proctor test is rarely used as a reference in such heterogeneous and unconventional materials as random fillings. The nuclear densimeter offers specific problems of the presence of rock, with the absence of fines, which does not allow the gamma radiation emitting stem to be introduced into the compacted layer in the presence of rock with medium–high hardness. Thus, the comparison with a reference Proctor loses interest due to its low representativeness, as it is mostly made with the less common fraction by replacing the larger sizes with fines, specifically those retained by the 20 mm sieve.

4. Conclusions

The maximum size of the random fill particles conditions the effectiveness of compaction tests such as in-situ density, modified Proctor, PBT, topographic settlements, and wheel tracking test. The new procedure revises the wheel tracking test and the topographical settlement test, optimizing the results. Finally, statistical analysis allows simplification of the quality control procedure for core slate random fillings, with a maximum layer thickness of 800 mm. An optimization of the compaction control system was achieved in random fillings core, obtaining a reduction in the control time.
The classical procedure by topographic settlement control is insufficient, and in the core of random fillings, adjustments were made to replace the topographic settlement and the wheel impression test by the PBT so that the control tests proposed as a new compaction quality control were the nuclear densities and the plate bearing test with a 600 mm diameter plate.

Author Contributions: Data curation, E.T.-L.-Z. and L.J.-G.; formal analysis, E.T.-L.-Z.; investigation, E.T.-L.-Z. and Á.V.-Z.; methodology, E.T.-L.-Z.; project administration, E.T.-L.-Z.; resources, E.T.-L.-Z.; software, E.T.-L.-Z. and L.J.-G.; supervision, E.T.-L.-Z., Á.V.-Z. and M.Á.C.-P.; validation, E.T.-L.-Z., Á.V.-Z. and M.Á.C.-P.; writing—original draft, E.T.-L.-Z.; writing—review and editing, E.T.-L.-Z., Á.V.-Z. and M.Á.C.-P. All authors have read and agreed to the published version of the manuscript.

Funding: This research received no external funding.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Not applicable.

Conflicts of Interest: The authors declare no conflict of interest.

The contributions of the research are:

- The nuclear methods have a low efficiency, limited by a maximum test thickness of 30 cm and the high variability of the materials;
- The PBT (φ 300 mm) provides unreliable results in the core of random fillings, with maximum sizes up to 500 mm. This research has demonstrated optimal control using PBT (φ 600 mm);
- The PBT (φ 600 mm) is proposed as the most representative test to define the degree of compaction in the new control method on core of slate random fillings. As this test is strongly associated with surface moisture, it should be carried out in the same area of validity as the optimum moisture obtained in the modified Proctor;
- New procedures for topographical settlement control and wheel impression tests were applied with optimal results to the core of random fillings formed by slates with maximum layer thicknesses of 800 mm;
- Statistical correlations were found between different compaction tests, which made it possible to eliminate redundant tests, thus optimizing quality control and construction procedures;
- The wheel tracking test can be deduced from the adjustment model for values between 1.5 ≤ h ≤ 4 mm. The limitations of the nuclear methods made it impossible to relate to other tests. Finally, the topographic seat control can be replaced for values of the PBT modules between 20 ≤ Ev1 ≤ 100 and 140 ≤ Ev2 ≤ 240;
- In the core of random fillings, including foundations and shoulders, which are formed by slates laid in layers with a maximum thickness of 800 mm, considering all the factors described in this research and summary in the discussion and conclusions, it is proposed as a quality control of the compaction to carry out PBT tests (φ 600 mm) and the in situ determination of density and moisture content by nuclear methods.

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