Angular momentum-large-scale structure alignments in $\Lambda$CDM models and the SDSS

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ABSTRACT
We study the alignments between the angular momentum of individual objects and the large-scale structure in cosmological numerical simulations and real data from the Sloan Digital Sky Survey, Data Release 6 (SDSS-DR6). To this end, we measure anisotropies in the two point cross-correlation function around simulated haloes and observed galaxies, studying separately the one- and two-halo regimes. The alignment of the angular momentum of dark-matter haloes in $\Lambda$ cold dark matter ($\Lambda$CDM) simulations is found to be dependent on scale and halo mass. At large distances (two-halo regime), the spins of high-mass haloes are preferentially oriented in the direction perpendicular to the distribution of matter; lower mass systems show a weaker trend that may even reverse to show an angular momentum in the plane of the matter distribution. In the one-halo term regime, the angular momentum is aligned in the direction perpendicular to the matter distribution; the effect is stronger than for the one-halo term and increases for higher mass systems.

On the observational side, we focus our study on galaxies in the SDSS-DR6 with elongated apparent shapes, and study alignments with respect to the major semi-axis. We study five samples of edge-on galaxies; the full SDSS-DR6 edge-on sample, bright galaxies, faint galaxies, red galaxies and blue galaxies (the latter two consisting mainly of ellipticals and spirals, respectively). Using the two-halo term of the projected correlation function, we find an excess of structure in the direction of the major semi-axis for all samples; the red sample shows the highest alignment (2.7 ± 0.8 per cent) and indicates that the angular momentum of flattened spheroidals tends to be perpendicular to the large-scale structure. These results are in qualitative agreement with the numerical simulation results indicating that the angular momentum of galaxies could be built up as in the Tidal Torque scenario. The one-halo term only shows a significant alignment for blue spirals (1.0 ± 0.4 per cent), consistent with the one-halo results from the simulation but with a lower amplitude. This could indicate that even though the structure traced by galaxies is adequate to study large-scale structure alignments, this would not be the case for the inner structure of low-mass haloes, $M \leq 10^{13} h^{-1} M_\odot$, an effect apparently more important around red $g - r > 0.7$ galaxies.

Key words: methods: numerical – methods: statistical – galaxies: formation – large-scale structure of Universe.

1 INTRODUCTION
In the current paradigm of large-scale structure formation in the Universe, it is well established that the angular momentum of dark-matter (DM) haloes is determined early in the history of the Universe by the gravitational interaction between the quadrupole of the collapsing proto-halo region and the surrounding matter. This was first formulated for the hierarchical theory of structure formation by White (1984), Doroshkevich (1970) and Peebles (1969), and it is claimed that this is a natural consequence of the perturbative treatment of the gravitational instability scenario (Porciani, Dekel & Hoffman 2002a). Several inherent properties to the tidal torque process (Tidal Torque Theory, TTT) have been noticed and studied in the literature. For instance, it is expected from TTT, and also supported to some degree by $N$-body simulations, that the
angular-momentum starts growing linearly with time (Peebles 1969; White 1984; Catelan & Theuns 1996b), and that later on this process looses efficiency after the halo turn-around. This is due to the reduction of halo inertia by collapse, and to the continued expansion of the neighbouring matter responsible for the tidal torque.

There are several analytic studies of the TTT scenario (Peebles 1969; Doroshkevich 1970; White 1984; Hoffman 1986; Heavens & Peacock 1988; Catelan & Porciani 2001), as well as semi-analytic approaches (Catelan & Theuns 1996a) and fully non-linear work using cosmological simulations (Barnes & Efstathiou 1987; Nagashima & Gouda 1998; Sugerman, Summers & Kamionkowski 2000; Porciani, Dekel & Hoffman 2002a,b; Peirani, Mohayaee & de Freitas Pacheco 2004). The agreement is that the resulting halo population is poorly rotationally supported; the velocity dispersion at virialisation is found to be the most important mechanism for halo equilibrium. As a result, the distribution of spin parameters is lognormal which peaks at quite low values, \( \lambda_{\text{med}} \approx 0.035 \) (Bullock et al. 2001; Gardner 2001; D’Onghia & Burkert 2004; Macciò et al. 2006; Bett et al. 2007). Unfortunately, it is not possible to obtain a direct measurement of spin parameters in actual galaxies. Despite this, Hernandez et al. (2007) used indirect methods to derive distributions of galaxy spin parameters consistent with theoretical predictions.

From an observational point of view, it can be easier in some cases to determine the direction of the angular momentum of a given galaxy rather than its amplitude. There has been a recent increase in the interest concerning the possibility of galaxy alignments with the large-scale structure. Such studies are important to test the already well-developed TTT, and to assess the possibility that such correlations affect the results of cosmic shear measurements. Regarding the former, TTT produces noisy predictions due to the non-linear nature of the accretion processes of clumpy matter (Porciani et al. 2002a; Vitvitska et al. 2002), on scales below the coherent scale of flows predicted by linear theory. The second tests for the effects on cosmic shear studies used to analyse weak lensing, may answer whether there is an intrinsic alignment in the structure traced by galaxies that could result in a spurious contribution to the shear power spectrum (Croft & Metzler 2000; Catelan, Kamionkowski & Blandford 2001; Crittenden et al. 2001; Brown et al. 2002; Jing 2002; Heymans & Heavens 2003; King & Schneider 2003; Takada & White 2004; Heymans et al. 2004; King 2005; Bridle & Abdalla 2007; Hirata et al. 2007). Several authors have searched for galaxy alignments in the super-galactic plane (de Vaucouleurs 1953; Flin & Godlowski 1989; Garrido et al. 1993; Sugai & Tye 1995; Hu et al. 1998, 2006), extending out to several tens of megaparsecs from our Galaxy, and more recently on large galaxy surveys (Hirata et al. 2004; Mandelbaum et al. 2006; Hirata et al. 2007; Lee & Erdogdu 2007; Lee & Pen 2007). Lee & Erdogdu (2007) claim a direct evidence of an alignment between galaxy position angle in 2MRs (the 2MASS Redshift Survey) and the tidal field deduced from galaxy positions.

An interesting approach to the analysis of galaxy alignments is to use the radial direction to the centres of voids as characteristic directions in the large-scale structure. It is well known that as they evolve, large voids tend to be rounder, behaviour which is opposite to that shown by bound structure. Negative density perturbations in the initial-fluctuation field that will later become voids, are characterized by a decreasing asphericity as the expansion of the Universe proceeds, as is shown by Sheth & van de Weygaert (2004) (and references therein). Taking advantage of this particular characteristic of voids, it is possible to study the whether galaxy or halo angular momenta are aligned with the void shells just by considering the angle with respect to the direction to the void centre. This is the approach used by Trujillo, Carretero & Patrii (2006) applied to the SDSS and two-degree field galaxy redshift survey (2dFGRS), and by Bruno et al. (2007), Cuesta et al. (2008) and Patiri et al. (2006) to numerical simulations. Trujillo et al. (2006) find with a high level of confidence that spiral galaxies located on the shells of the largest cosmic voids have rotation axes that lie preferentially on the void surface, in agreement with the simulation results of Bruno et al. (2007), Cuesta et al. (2008) and Patiri et al. (2006). Other more general methods that also take into account alignments with large-scale filaments in numerical simulations show similar results (Aragon-Calvo et al. 2007; Hahn et al. 2007a,b).

In this paper, we present results from a study of alignments between individual objects and their surrounding structure in quantitative concordance with TTT predictions and previous observational results. We use a novel approach to study alignments with the large-scale structure using as a reference the galaxy/DM halo angular momentum. Using numerical simulations, we study alignments predictions in a cold dark matter model with a cosmological constant (\(\Lambda\)CDM), and compare such predictions with the results obtained from the Sloan Digital Sky Survey, Data Release 6 (SDSS-DR6, Adelman-McCarthy et al. 2008). To this end, we use the galaxy two-point correlation function applied both, in its three-dimensional definition to the full-numerical simulation and in its projected version to mimic the observational limitations. The latter allows us to determine that we should be able to detect the expected low-signal alignments, even in small galaxy samples. This allows us to measure the alignment of galaxies and haloes over wide ranges in mass and separation, and also to quantify the dependence of this alignment on halo mass, galaxy colour and luminosity.

This paper is organised as follows. Section 2 presents the numerical simulation and the statistical tools we will use in this work; it also presents an analysis of the impact of the observational biases on the detection of alignments. Section 3 contains the analysis of observational samples of galaxies from the SDSS. The comparison between models and observations as well as the discussion of the results is presented in Section 4, and Section 5 contains the final conclusions from this work.

2 Anisotropies in the Three-Dimensional Correlation Function

In this section, we analyse the three-dimensional two-point correlation function, using cluster-particle pairs, measured using \(\Lambda\)CDM numerical simulations, taking into account the orientation with respect to the centre halo angular momentum. To this end, we have run two periodic simulations of 500 and 60 \(h^{-1}\) Mpc computational box sizes, for a flat low-density universe, with a matter density \(\Omega_m = 1 - \Omega_{\Lambda} = 0.3\), Hubble constant \(H_0 = 70\) km s\(^{-1}\) Mpc\(^{-1}\) and normalization parameter \(\sigma_8 = 0.8\). The particle resolutions are \(m_p \approx 7.2 \times 10^{10} h^{-1} M_{\odot}\) for the large simulation, and \(m_p \approx 1.2 \times 10^6 h^{-1} M_{\odot}\) for the small one. The identification of particle clumps has been carried out by means of a standard friends-of-friends algorithm with a percolation length given by \(l = 0.17 \bar{v}^{-1/3}\), where \(\bar{v}\) is the mean number density of DM particles. Both simulations
have been performed using the first version of the GADGET code developed by Springel, Yoshida & White (2001). We consider haloes with at least 30 and 100 particles in the large and small simulations, respectively, in order to ensure an accurate measurement of the halo angular momentum.

The spatial halo-particle cross-correlation function $\xi(r)$ which we will use in this section, measures the excess probability with respect to a random distribution, that a DM particle will reside at a distance $r$ away from a given halo centre, in the volume element $dV$.

$$dP = \bar v [1 + \xi(r)] dV.$$  

(1)

A standard method to measure $\xi(r)$ in a simulation box is to count pairs at a given distance bin, and then normalize this number by the expected number of pairs for a constant number density of objects. In our measurements, we perform these counts stacking pairs depending on the angle between their position relative to the centre halo and its angular momentum. We consider tree cases, (i) using all pairs regardless of this angle (spherical shell volumes, isotropic case), (ii) using all pairs subtending an angle from the angular momentum less than a given threshold $\theta_1$ (parallel case), and (iii) adding pairs at lower inclinations than a limit angle $\theta_2$ from the perpendicular plane to the angular momentum (perpendicular case).

We choose the threshold angles, for the parallel and perpendicular cases mentioned above ($\theta_1$ and $\theta_2$, respectively), so that the volumes in each case are the same. This can be achieved by setting, $\sin(\theta_2) = 1 - \cos(\theta_1) = \chi$, and choosing a value for the threshold parameter $\chi$. Selecting $\chi \leq 0.5$ implies angles $\theta_1 \leq 60^\circ$ and $\theta_2 \leq 30^\circ$. Throughout this paper, we use $\chi = 0.5$.

Errors in the correlation function are estimated using the jackknife technique, with a total of 50 subsamples for the numerical simulation (20 jacknifes for the SDSS data analysis). We find that our errors are stable for this number of jackknife subsamples (we tested from 20 to 100) and do not produce underestimations. In the case of quotients between correlation functions, we apply the jackknife technique to the actual measurement of the ratio. We adopt the jackknife technique since it has been reported to provide similar error estimates to those obtained from independent samples (see for instance, Padilla et al. 2004).

2.1 Simulation results

The analysis of alignments of structure with the angular momentum of DM haloes presents a first difficulty in that in order to obtain a reliable and stable direction for the halo spin, it is often necessary to use a large number of particles per halo. We find that using 30 particles provides reasonable results, but this imposes a rather high lower limit to halo masses of $2.2 \times 10^{13} h^{-1} M_\odot$ for the large simulation, and $3.6 \times 10^9 h^{-1} M_\odot$ for the smaller one. We analysed the distribution of angular momentum parameters and find that the reported high $\lambda$ tail (Bett et al. 2007) due to low number of particles per halo, is not present in any of our samples of DM haloes. We notice that the clustering signal in the small simulation on large scales may be affected by the small box size.

From this point on, we will centre most of our analysis on samples of DM haloes with different masses. From the small simulation, we draw four DM halo subsamples separating haloes of different mass starting at a minimum of 100 particles or $M \geq 1.2 \times 10^{10} h^{-1} M_\odot$ (the lowest mass sample considered includes haloes of up to 300 particles each; we do not use haloes of lower masses even though we are still above the minimum number of particles, we consider safe to consider). Nine samples are drawn from the large simulation and contain DM haloes with more than 30 particles. The subsample with the most massive haloes starts at 1000 particle members corresponding to $M \geq 7.2 \times 10^{13} h^{-1} M_\odot$.

The left-hand panels of Fig. 1 show the cross-correlation function between low-mass DM haloes and DM particles (top left) in the directions parallel and perpendicular to their angular momenta, and in all directions (diamonds, triangles and squares, respectively). The lower panel shows the ratios between these three estimates and the correlation function considering all neighbours; their relative amplitudes help to identify alignments in either direction. As can

![Figure 1](https://academic.oup.com/mnras/article-abstract/389/3/1127/1016872/1129)
be seen, the relative amplitudes of the correlation function when using neighbours in the directions parallel and perpendicular to the angular momentum of the DM halo are different; for small separations \( R < 1 h^{-1} \text{Mpc} \), there is an excess of correlation in the direction perpendicular to the angular momentum of up to a 20 per cent effect (between correlations parallel and perpendicular to the angular momentum, lower panel), whereas for larger separations the alignment diminishes and shows a tendency to reverse (although, as can be seen in figure, errors are larger at these separations); we come back to this later in this section where we use a higher signal estimator for alignments.

When using higher mass DM haloes, the effect is also present with an even higher difference and statistical significance between the structure in the direction of the angular momentum and perpendicular to it (right-hand panels of Fig. 1). In this case, neighbours in the direction perpendicular to the angular momentum show more correlation, and there is a clear tendency for this alignment to decrease with separation, which goes from almost a 50 per cent effect on relative amplitudes (lower panel) at small separations to about <5 per cent at large separations. Note that the alignment does not change at large separations as seemed to be the case for low-mass haloes, even at \( R = 20 h^{-1} \text{Mpc} \) compared to \( R = 5 h^{-1} \text{Mpc} \) analysed in the low-mass halo sample.

Notice that the halo-particle cross-correlation functions in Fig. 1 show the characteristic one- and two-halo terms reported in several previous measurements of both observational (e.g. Zehavi et al. 2004; Cooray 2005) and numerical simulations (Zheng et al. 2005); these two regimes are separated in figure by the vertical–dashed lines. This separation is obtained by measuring the scale at which the correlation function is seen to shift between these two regimes (there is a local minimum in the first derivative of the correlation function). It can be seen that the alignment signal shows a clear transition from the one- to the two-halo regime; in particular, low-mass haloes show indications of a different angular-momentum–large-scale alignment behaviour in the two-halo regime, suggesting an important relationship between alignment and halo term. This can be interpreted as different physical mechanisms producing the alignment in the one- and two-halo terms.

We make quantitative estimates of the alignments for the one- and two-halo terms separately from the cross-correlation functions shown in Fig. 1 as well as from the other samples of DM haloes with intermediate masses (for a total of 13 samples of varying halo masses). We only consider pairs that are separated by a distance at least as large as the transition between regimes for the two-halo term, and at shorter separations for the one-halo calculations.

In order to avoid effects of covariance between the correlation-function bins to some extent, we make global one- and two-halo term estimates of the ratios between the correlation functions in the directions perpendicular and parallel to the angular momentum of haloes, using all the halo-particle pairs separated by distances within the one- and two-halo ranges (i.e. we do not use the narrow bins in \( \log_{10}(r) \) used to calculate the cross-correlation functions). We acknowledge that traces of covariance will still be present between the one- and two-halo term ratios. We present these results in Fig. 2, where triangles show the one-halo term ratio between correlation functions for neighbours in the directions perpendicular and parallel to the halo angular momentum; diamonds correspond to the two-halo term. The horizontal long-dashed line at \( \xi_\parallel/\xi_\perp = 1 \) corresponds to the isotropic case. The data-points at masses lower than \( 10^{12} h^{-1} \text{M}_\odot \) correspond to the small numerical simulation, and show larger errors due to both, the smaller simulated volume, and the lower amplitude of clustering characterizing low-mass haloes.

As can be seen, the one-halo term always shows more structure in the direction perpendicular to the angular momentum, and more so for larger masses, whereas the two-halo term shows a similar behaviour with the possible exception of low-mass haloes, whose angular momenta tend to point in the direction of the large-scale structure (although with a low statistical significance). The alignments are detected at about a 5\( \sigma \) level for the higher mass halo subsamples drawn from the large simulation. As in the two-halo regime, low-mass haloes show considerably higher errors.

In the case of low-mass haloes (\( M \approx 10^{10} h^{-1} \text{M}_\odot \)) in the two-halo term regime (diamonds in Fig. 2), the alignment signal is the opposite to that of higher mass haloes (a 10 \( \pm \) 5 per cent effect). This anti-alignment signal fits well with the overall tendency for this quotient \( \xi_\parallel/\xi_\perp \) to increase with mass, which can be fit by a log-linear relation which crosses the unit value at \( M \approx 10^{12} h^{-1} \text{M}_\odot \). This mass limit suggest a change in the alignment signal in qualitative agreement (regarding the alignment direction) with results on simulations by Hahn et al. (2007a), with masses above and below the typical mass scale for collapse \( M_* = 5.5 \times 10^{12.5} h^{-1} \text{M}_\odot \) at \( z = 0 \). The best-fitting log-linear relation for the two-halo term results is shown in Fig. 2 (dash–dotted line), and corresponds to,

\[
\xi_\parallel/\xi_\perp = (0.95 \pm 0.01) + (0.082 \pm 0.008)[\log_{10}(M) - 11.5].
\]

(2)

For the one-halo term, the dependence of alignment on mass is well adjusted by (dashed line on Fig. 2),

\[
\xi_\parallel/\xi_\perp = (0.95 \pm 0.01) + (0.082 \pm 0.008)[\log_{10}(M) - 11.5].
\]

(3)

The two-halo term effect can be understood within the framework of TTT, specially for the high-mass haloes, which readily show that their angular momentum is perpendicular to the present-day mass distribution. It seems that for high enough mass haloes, the local large-scale structure still describes the original tidal field. In the case of low-mass haloes, the alignment seems to reverse. This result can be understood by an intuitive non-linear effect beyond the abilities of TTT, for example if these haloes have formed recently in filaments, from the merger of material arriving from voids surrounding these elongated structures.
The one-halo term results indicate that regardless of halo mass, the structure within DM haloes is preferentially aligned with the plane perpendicular to the angular momentum, with a higher statistical significance and signal than the two-halo term.

2.2 Simulating observational biases in the numerical simulation

It can be difficult to estimate the angular momentum of real galaxies. In the case of the SDSS-DR6, which we use in this work, the only information that can allow us to obtain an estimate of the direction of the angular momentum is the photometry of galaxy images, specially for spiral galaxies but also for ellipticals. We assume that spiral discs or flattened spheroids are perpendicular to the angular momentum of galaxies and therefore, edge-on galaxies (either discs or spheroidals) will be more likely to have their angular momentum on the plane of the sky. Then, one can calculate the cross-correlation function for neighbours in the projected direction parallel and perpendicular to the direction of the angular momentum of the centre galaxies, in redshift slices around them, assuming all these neighbours to be at the same distance than the centre galaxy. This slice needs to be defined so that it avoids projecting large amounts of foreground and background structures while still allowing enough numbers of neighbours to obtain good statistics.

In order to assess whether the alignments found in the previous subsection are identifiable in observational catalogues analysed this way, we reproduce the procedure mentioned in the previous paragraph in our analysis of the numerical simulation which consists on projecting the structure on the plane of the sky, assuming all objects within $\Delta v = 750 \text{ km s}^{-1}$ from the centre haloes to be exactly at the same distance from the observer.

Therefore, we only use information from two Cartesian coordinates in the simulation, $x$ and $y$, and transform the third, $z$, into a velocity component by multiplying $z$ by the Hubble constant and adding the $z$ component of the peculiar velocity. In order to complete the emulation of redshift space effects suffered by observational surveys, we apply this transformation to the simulation particles as well as to the halo catalogue. We then select ‘edge-on’ haloes from the simulation, by requiring that their angular momentum is at an angle less than 60° from the sky, represented by the $x-y$ plane. We can then study two projected correlation functions centred in these objects using DM particles, (i) a correlation function calculated using pairs that subtend an angle with the projected angular momentum of less than 30°, which we call the parallel projected correlation function ($\omega_{||}$), and (ii) a perpendicular projected correlation function ($\omega_{\perp}$) obtained by counting pairs that subtend an angle greater than 60° from the projected angular momentum.

Fig. 3 shows the results from this procedure. The left-hand panels show the results for low-mass haloes in the small simulation (projected correlation functions in the top left, and ratios in the bottom left), whereas the right-hand panels show the results for high-mass haloes in the large simulation. As can be seen, these results are qualitatively consistent with the alignment signal found in the previous subsection using the full three-dimensional correlation function, which indicates that projected correlation functions are a suitable tool to detect this effect. The overall effect has a lower amplitude; high-mass haloes show a ratio between structure in the directions perpendicular and parallel to their angular momenta of about a 30 per cent excess (for the three-dimensional case, this was above 50 per cent) and low-mass haloes show a 10 per cent effect (compared to 20–30 per cent), which makes this detection a slightly more difficult task.

3 OBSERVATIONS

Galaxies with spiral and flattened spheroidal shapes projected on to the sky give a handle on their orientation with respect to the line of sight and, therefore, it is possible to estimate in a statistical sense the direction of their angular momentum. Spiral galaxies with round projected shapes are likely discs seen face-on and therefore their

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\(^2\) Such angle threshold is equivalent to a ratio of 0.5 of the ellipsoidal image semi-axes for a perfect thin disc.
angular momenta point in the direction perpendicular to the plane of the sky; elongated projected shapes indicate discs seen edge-on, and therefore their angular momenta point in the direction perpendicular to the long axis of the ellipsoid. On the other hand, elliptical galaxies with round projected shapes can either be nearly intrinsically spherical or flattened spheroids seen face-on; however, elongated ellipticals are more likely flattened spheroids seen edge-on since recent results on intrinsic elliptical shapes indicate that these are more commonly oblate rather than prolate spheroids (e.g. Padilla & Strauss 2008). Therefore, elongated ellipticals are likely to be also characterized by angular momenta pointing in the direction of the plane of the sky roughly perpendicular to the major axis of the ellipsoid, as is the case for edge-on spiral galaxies. These last two types of galaxies will be the centre of the following analysis. We notice that the amplitude of the angular momentum of flattened spheroidal is likely to have a low amplitude relative to that of spiral galaxies.

The sample we selected to carry out our analysis is the spectroscopic SDSS-DR6, which contains a total of ≈580 000 galaxies with spectroscopic redshifts and photometry in five bands, u, g, r, i, z, as well as parameters determining the projected galaxy shapes consisting of the two semi-axes and the position angle of the ellipse that once convolved with the point spread function (seeing) provides the best match to the photometric image of each individual galaxy. In the remainder of this paper, we only consider SDSS-DR6 galaxies within the redshift range 0.02 < z < 0.09.

We study the alignment signal in the observational data for different subsamples defined by galaxy colour and luminosity in order to detect trends that can be associated to the results from the numerical simulation. The subsamples we study are sample O1, consisting of all the edge-on galaxies with axial ratio b/a < 0.7 in the SDSS-DR6; O2, red galaxies with g − r > 0.7; O3, blue galaxies with g − r < 0.7; O4, faint galaxies with M_r > −19.5; and O5 composed by bright galaxies with M_r < −19.5. The selection of subsamples is done so as to ensure a number of target galaxies to allow good statistics (>1000); the number of galaxies in each sample is shown in Table 1, where we also show the galaxy number density calculated out to the redshift of completeness of each sample.

In order to characterize in a quantitative way the subsamples selected from the SDSS-DR6, we calculate the median mass of ΛCDM haloes predicted to show the same two-halo regime clustering amplitude as the galaxies in each subsample. We follow the procedure used in several previous works (cf. Croft, Dalton & Efstathiou 1999; Padilla et al. 2001) consisting on calculating the auto-correlation function of galaxies in two coordinates, one parallel (σ) and one perpendicular (π) to the line of sight, ξ(σ, π), and integrating over the π direction to avoid the effect of redshift space distortions. The result from this integration is the projected correlation function (see for instance, Croft et al. 1999), Ξ(σ),

$$\Xi(\sigma) = 2 \int_{\min}^{\max} \xi(\sigma, \pi) d\pi,$$

(4)

which in turn can be inverted to obtain the real-space correlation function via

$$\xi(r) = \frac{-1}{\pi} \sum_{j=0}^{\infty} \frac{\Xi(\sigma_{j+1}) - \Xi(\sigma_j)}{\sigma_{j+1} - \sigma_j} \ln \left( \frac{\sigma_{j+1} + \sqrt{\sigma_{j+1}^2 - \sigma_j^2}}{\sigma_j + \sqrt{\sigma_j^2 - \sigma_j^2}} \right).$$

(5)

where the sum is performed over the bins in $\sigma$ where the projected correlation function has been calculated. The masses of host haloes can then be obtained by finding the bias between the resulting real-space correlation functions and the matter correlation functions in a ΛCDM cosmology (both in the two-halo regime), which we obtain by Fourier transforming the non-linear matter power spectrum (from Peacock & Smith 2000) for the same cosmological parameters used in the numerical simulations. With an estimate of the bias, the mass of the host haloes can be found by using the Sheth et al. (2001) formalism. Note that this procedure is equivalent to measure the real-space halo–halo correlation function for haloes of different masses (Sheth et al. 2001; Padilla & Baugh 2002), with the advantage of avoiding large uncertainties from small samples of haloes restricted to narrow ranges of halo mass in the simulation. We show one example of this procedure in Fig. 4, where we find the mass of haloes with an equivalent clustering amplitude to the sample of red galaxies in the SDSS-DR6 (O2). In this figure, the top panel shows the auto-correlation function, $\xi(\sigma, \pi)$, of O2 galaxies, and the lower panel the resulting real-space correlation function (symbols) and the best-fitting ΛCDM curve. From this analysis, we find that red galaxies in the SDSS-DR6 (with b/a < 0.7) are consistent with haloes of a median mass of log_{10}(M/h^3 M_☉) = 13.06±0.19. This provides us with a quantitative way to compare the SDSS-DR6 subsamples to the halo samples in the numerical simulations. Also, in order to infer this scale for our observational samples, we will use the dependence of the one- to two-halo term transition on DM halo mass measured in our numerical simulations.

The other SDSS-DR6 galaxy samples are fitted by the correlation function of DM haloes of masses indicated in Table 1. Notice that our study covers over one and a half decades in the host-halo mass of SDSS-DR6 galaxies.

As we demonstrated in the previous section both, the large-scale structure and alignments surrounding galaxies, can be studied using the projected correlation function, $\omega(\sigma)$, measured in terms of the projected separation, $\sigma$. We now apply this method to our samples of edge-on galaxies, and compare the outcome from using tracers in the direction parallel and perpendicular to the inferred angular momentum, to detect differences between the structures along these two directions.

The projected correlation functions are calculated using galaxies in a given subsample, cross-correlated to the full spectroscopic SDSS-DR6 catalogue. As in the two-dimensional analysis carried out in the numerical simulations, we calculate the cross-correlation for edge-on galaxies selected so that b/a < 0.7. Note that in the numerical simulation, we used an angle between the halo angular momentum and the line of sight of 60°, which in the case of a perfect thin disc is equivalent to b/a = 0.5, but is larger for a thick disc as is the case of the intrinsic shapes of spiral galaxies or flattened ellipsoids (Padilla & Strauss 2008).

Fig. 5 shows the measured correlation functions for Edge-on galaxies for the three subsamples that show significantly different

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Table 1. Observational samples from the SDSS-DR6 spectroscopic main galaxy sample. The first and second column indicate the sample name and number of galaxies in them, the third column indicates the number density, and the fourth column the host-halo mass.

| Sample | Members | n/10^3 h^{-3} Mpc^{-3} | Log_{10}(M_{host}/h^{-1} M_☉) |
|--------|---------|------------------------|-------------------------------|
| O1     | 132000  | 10.4 ± 0.8              | 12.56±0.30                   |
| O2     | 59300   | 6.50 ± 0.12             | 13.06±0.19                   |
| O3     | 72700   | 5.50 ± 0.12             | 11.40±0.56                   |
| O4     | 10900   | 7.15 ± 0.17             | 12.19±0.45                   |
| O5     | 1400    | 1.10 ± 0.20             | 12.67±0.28                   |
signatures of alignments with the angular momentum. These are the full sample of edge-on spirals, O1 (top panel), the red galaxy sample, O2 (middle panel) and the blue galaxies, sample O3 (bottom panel). As in the results for the numerical simulation, triangles show the correlation with galaxies in the direction of the angular momentum, diamonds in the perpendicular direction, and squares, when using all neighbours. A first glance at the shapes of these correlation functions indicates that there is not as clear a transition between the one- and two-halo terms as in the results from the numerical simulations (see Fig. 3); in these samples the main effect is a transition to a roughly constant slope for the log(ξ) versus log σ relation. This may be an indication that the internal structure of haloes is not traced in the same way by galaxies in the SDSS-DR6 and DM particles in the ΛCDM model. Regarding the alignments, it can be seen that the three subsamples show the large-scale structure preferentially aligned with the direction perpendicular to the angular momentum, specially for the two-halo regime, as was found in the cosmological simulation. The difference between the two correlation functions is roughly a 2σ detection over the range of scales defined by $2 < r/h^{-1}\text{Mpc} < 20$ and corresponds to about a 2–4 per cent effect.

The analysis of the faint and bright samples (O4 and O5, respectively) provides alignment results in quantitative agreement with the full galaxy sample, O1, with results within a 1σ difference.

**Figure 4.** Top panel: correlation function around ‘edge-on’ red spiral galaxies in the SDSS-DR6 (sample O3), in the directions parallel and perpendicular to the line of sight. The colour indicates the amplitude of the correlation function (see the figure key). Bottom panel: real-space correlation function for the same sample of galaxies, obtained as explained in the text (symbols with errorbars), and the best-fitting ΛCDM real-space correlation function (black lines). The dashed lines show the range of correlation function amplitudes allowed by the errors in the data. The gray thick line shows the mass real-space correlation function in the ΛCDM model.

**Figure 5.** Correlation functions around ‘edge-on’ galaxies in the SDSS-DR6, in the direction perpendicular and parallel to the angular momentum of centre haloes (triangles and diamonds, respectively). Top panel corresponds to sample O1 (full SDSS-DR6), middle panel to O2 (red galaxies), and bottom panel to sample O3 (blue galaxies). The vertical–dashed lines show the transition from the one- to the two-halo regimes corresponding to the host-halo mass obtained from the real-space correlation function of the different samples.

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Therefore, we will not show results from these two samples in the remainder of this work.

A more quantitative comparison between observational and simulation results is presented in the following section.

4 DISCUSSION

In order to compare quantitatively the alignments found in the observations and in the numerical simulation, we use the transition scale from the one- to two-halo regimes inferred in the previous section to determine the degree of alignment found in these two regimes separately. As in section 2.1, we estimate ratios between the correlation functions in the directions perpendicular and parallel to the estimated galaxy angular momentum direction, using all pairs within the one- and two-halo regimes. This can then be directly compared to the results from the numerical simulations for projected correlations.

Fig. 6 shows the ratios between projected correlation functions in the directions parallel and perpendicular to the angular momentum as a function of halo mass. The results from the numerical simulations are shown as diamonds, and the results from the observational samples at the corresponding host-halo masses are shown as filled symbols. We show results for samples O1 (full SDSS-DR6, filled squares), O2 (red galaxies, filled upward pointing triangles) and O3 (blue galaxies, filled downward pointing triangles). The top panel shows the results from the analysis of the one-halo term, the lower panel from the two-halo term. For the two-halo term regime, the resulting alignment signals for observational samples are $1.8 \pm 0.5$ per cent for the full sample O1, $2.7 \pm 0.7$ per cent for the red galaxy sample O2 and $0.8 \pm 0.4$ per cent for the blue galaxy sample O3. The one-halo term regime shows alignments of $0.1 \pm 0.5, 0.1 \pm 0.5$ and $1.0 \pm 0.4$ per cent for samples O1, O2 and O3, respectively. As can be seen, the alignment found in the two-halo term is consistent between observational samples and the numerical simulation (differences are at a maximum a 1σ effect).

This agreement indicates that TTT in combination with hierarchical clustering is a viable theory since not only the angular momentum of galaxies points in the direction perpendicular to the surrounding large-scale structure, but also the amplitude of the effect is similar to what is found in the numerical simulations. It should be noticed that this would also indicate that the direction of the angular momentum in galaxies in these samples is tracing the angular momentum of the host halo. The results for the one-halo term, on the other hand, show that galaxies follow a different behaviour than DM haloes as was suspected from the lack of a clear transition to the one-halo term in the shape of the SDSS projected correlation functions; at the range of masses corresponding to the observational samples, the simulated haloes show very significant alignments, whereas the only sample of galaxies that shows non-zero alignment is that composed by blue galaxies (although still lower than the simulation data, at a regime of low-expected alignments). The combination of the one- and two-halo term results could indicate that the general galaxy population in the SDSS-DR6 which our samples are cross-correlated to, can be used as good tracers of the large-scale structure (i.e. have not suffered important changes to deviate from the angular momentum of their host haloes) but would fail to serve as indicators of the internal distribution of matter in their host DM haloes; different astrophysical processes could produce this effect, specially for such low $M \approx 10^{13} h^{-1} M_{\odot}$ halo masses.\footnote{This result is particularly interesting since blue galaxies do show traces of an alignment in the same direction as the numerical simulation, which has a number of possible explanations. For instance, the angular momentum of red galaxies could be subject to a reshuffle that adds enough noise to loose its alignment with the internal halo structure while leaving the large-scale signal almost intact, an effect could also involve a positional reshuffle within the halo structure; another possibility is that red galaxies are able to rearrange their companion galaxies inside DM haloes. However, a more quantitative comparison between observational and simulation results is presented in the following section. This agreement indicates that TTT in combination with hierarchical clustering is a viable theory since not only the angular momentum of galaxies points in the direction perpendicular to the surrounding large-scale structure, but also the amplitude of the effect is similar to what is found in the numerical simulations. It should be noticed that this would also indicate that the direction of the angular momentum in galaxies in these samples is tracing the angular momentum of the host halo. The results for the one-halo term, on the other hand, show that galaxies follow a different behaviour than DM haloes as was suspected from the lack of a clear transition to the one-halo term in the shape of the SDSS projected correlation functions; at the range of masses corresponding to the observational samples, the simulated haloes show very significant alignments, whereas the only sample of galaxies that shows non-zero alignment is that composed by blue galaxies (although still lower than the simulation data, at a regime of low-expected alignments). The combination of the one- and two-halo term results could indicate that the general galaxy population in the SDSS-DR6 which our samples are cross-correlated to, can be used as good tracers of the large-scale structure (i.e. have not suffered important changes to deviate from the angular momentum of their host haloes) but would fail to serve as indicators of the internal distribution of matter in their host DM haloes; different astrophysical processes could produce this effect, specially for such low $M \approx 10^{13} h^{-1} M_{\odot}$ halo masses.\footnote{There is observational evidence that groups of galaxies with masses above this limit are characterized by intrinsic shapes consistent to those found in numerical simulations (Paz et al. 2006); however, it is difficult to directly measure the shapes of lower mass systems due to discreteness effects.}
more quantitative analysis is required in order to find the true underlying cause for this behaviour. We acknowledge the possibility that observational biases not included in our analysis of the numerical simulation are still affecting these measurements.

5 CONCLUSIONS
We study the alignments between the angular momentum of individual objects and the large-scale structure in cosmological numerical simulations and in the SDSS-DR6. The angular momentum of DM haloes in \( \Lambda \)CDM simulations is found to be preferentially oriented in the direction perpendicular to the distribution of matter in the range of separations corresponding to the one- and two-halo terms. These results are in agreement with the TTT.

We find that more massive haloes show a higher degree of alignment, and that the one-halo term shows a much higher alignment than the two-halo term. We find a maximum one-halo alignment of \( \sim 40 \) per cent for haloes of \( \gtrsim 10^{14} \, h^{-1} \, M_\odot \); at low masses, the one-halo signal seems to tend to a constant value of 20 per cent. The two-halo term alignment shows a maximum signal of \( \sim 15 \) per cent at high masses, and possible inversion at low masses where the angular momentum might even preferentially point in the direction of the distribution of mass on large scales. The latter would be consistent with low-mass groups formed not too long ago from mass distributed in the surrounding areas of the already-formed filaments or walls.

The alignment of the angular momentum with the large-scale structure found for low-mass systems is in agreement with previous works by (Trujillo et al. 2006) on redshift surveys, and by Brunino et al. (2007), Patiri et al. (2006), Cuesta et al. (2008), Aragon-Calvo et al. (2007), Hahn et al. (2007a) and Hahn et al. (2007b) on simulations. The main difference with these previous studies relies in that we quantify the strength of the alignment in terms of the two-point correlation function, as a function of halo mass. In particular, we find that a log-linear relation fits the dependence of alignment on halo mass, for both, the one- and two-halo term regimes. For the latter, we find that a log-linear relation fits the dependence of alignment on halo mass.

One-halo term results show either a null or lower alignment signal than expected from the analysis of projected correlations in the numerical simulation. This would suggest the effects of astrophysical processes acting so that galaxies do not follow the DM structure inside low-mass haloes of \( \lesssim 10^{13} \, h^{-1} \, M_\odot \) or lower masses, a result that complements previous studies of high-mass groups in the SDSS with \( \gtrsim 10^{13} \, h^{-1} \, M_\odot \), where galaxies are found to follow the internal DM structure (e.g. Paz et al. 2006). This effect is apparently more important for red, \( g - r > 0.7 \) galaxies, indicating that there may be interesting astrophysical effects at work at low-mass DM haloes which could produce changes in the orientation of galaxy angular momenta or the spatial redistribution of galaxies within them.

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Angular-momentum–LSS alignments

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