Compressed Sensing for THz FMCW Radar 3D Imaging

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A terahertz (THz) frequency-modulated continuous wave (FMCW) imaging radar system is developed for high-resolution 3D imaging recently. Aiming at the problems of long data acquisition periods and large sample sizes for the developed imaging system, an algorithm based on compressed sensing is proposed for THz FMCW radar imaging in this paper. Firstly, the FMCW radar signal model is built, and the conventional range migration algorithm is introduced for THz FMCW radar imaging. Then, compressed sensing is extended for THz FMCW radar 3D imaging, and the Newton smooth L0-norm (NSL0) algorithm is presented for sparse measurement data reconstruction. Both simulation and measurement experiments demonstrate the feasibility of reconstructing THz images from measurements even at the sparsity rate of 20%.

1. Introduction

Terahertz (THz) wave lies between infrared wave and millimeter wave, which is an electromagnetic wave that has not been fully recognized and utilized by human beings. Due to its ability of material penetration and harmless nonionizing radiation to human body, THz technology can be employed to effectively identify stealth and deceptive measures that cannot be distinguished by conventional means in the military fields and to identify concealed objects made of metal or inorganic materials for security check. As THz has a smaller wavelength and a wider bandwidth which will result in a higher resolution, THz imaging has been widely used in nondestructive inspections and medical diagnosis [1, 2]. With the rapid development of information countermeasures, antistealth, target search, and tracking, and materials science, THz imaging technology has made a great progress during the past decades.

Motivated by the huge application potential of high-resolution THz imaging technology, there has been growing interest in developing 3D imaging radar working at THz range. In 2007, a 220 GHz experimental frequency-modulated continuous wave (FMCW) inverse synthetic aperture radar (SAR) with a bandwidth of 8 GHz is designed to determine high-resolution scattering center distributions of targets [3]. A 240 GHz 3D FMCW imaging radar with a maximum bandwidth of 42 GHz is discussed in [4]. An imaging radar with the operation frequency of 580 GHz which is implemented in an all-solid-state design is developed at Jet Propulsion Laboratory (JPL) [5]. The first THz radar for fast standoff personnel screening with the operation frequency of 675 GHz is also built by JPL. A fast scanning device is designed to enable imaging at a frame rate of 1 Hz [6, 7]. An active FMCW imaging system ranging from 514 to 565 GHz (frequency centered at 540 GHz) is studied to image objects with a resolution of millimeter [8].

It can be found that THz 3D imaging is commonly realized with SAR technique, rather than building antenna arrays. This is due to that expensive devices in THz regime will lead to a high-cost imaging system having multiple transceivers. For a THz imaging system with SAR technique, the single transceiver is moved in a grid-like manner to produce an image with the processing approaches. Several SAR imaging algorithms in time domain, frequency domain,
and wavenumber domain have been proposed for THz FMCW SAR, respectively. A typical time domain back-projection algorithm is studied to obtain the image with 2D aperture synthesis for the SynView THz 3D imaging system [9]. A back-projection imaging approach has been presented in [10] for data processing of a 300 GHz imaging system. However, imaging algorithms in the time domain have a heavy calculation burden though they are able to process SAR data under a great variety of imaging geometries. A revised range-Doppler algorithm is presented for FMCW SAR imaging by compensating radar migration [11].

A nonlinear frequency-scaling algorithm is proposed by Meta SAR imaging by compensating radar migration [11]. A spatial aperture synthesis for the SynView THz 3D imaging system is introduced in Figure 2. And the RMA for THz FMCW radar imaging is given in Section 3. Section 4 describes the proposed 3D imaging algorithm based on compressed sensing that it can reconstruct signal from the sparse data samples.

The paper is organized as follows. The developed 220 GHz FMCW SAR imaging system is introduced in Section 2. And the RMA for THz FMCW radar imaging is given in Section 3. Section 4 describes the proposed 3D imaging algorithm based on compressed sensing. The experimental results are given and analyzed in Section 5 to verify the proposed imaging algorithm. The last section is Conclusion.

2. THz FMCW Imaging System

2.1. System Briefs. As shown in Figure 1, the FMCW THz imaging system developed in this paper consists of radio frequency transceiver subsystem, signal acquisition and processing subsystem, and planar scanning subsystem. When the THz FMCW imaging system works, an X-band FMCW signal generated through the direct digital synthesizer serves as the driving source of the transmission link which will output a THz FMCW signal. Then, the transmitted signal will be reflected by target and then received by the antenna. The received echoed signal is mixed with the reference signal to get the intermediate frequency (IF) signal which will be processed with the IF processing unit. Lastly, the processed IF signal is acquired with the data acquisition unit. The planar scanner controlled by the data acquisition and processing subsystem moves with a “stop-go-stop” manner. The echoed signals at certain points are acquired and stored by the processing software and are processed to generate 3D images after finalization of scanning. The picture of the developed THz FMCW imaging system is presented in Figure 2. And the specification parameters are illustrated in Table 1.

2.2. THz FMCW Signal Modeling. The transmitted signal of the THz FMCW imaging system can be expressed as

$$s(t) = \exp(jnk(t^2))\exp(j2\pi f_ct),$$

where $f_c$ denotes the central frequency, $T$ means the sweep duration, and $k$ is the chirp frequency rate. Assumed that the distance between the target and the radar is $R$, the echoed signal can be expressed as

$$s_r(t - \tau_R) = g \cdot \exp[jnk_r(t - \tau_R)^2] \exp[j2\pi f_c(t - \tau_R)],$$

where $\tau_R = 2R/c$ is the echoed signal delay and $g$ represents the target reflection coefficient. Dechirp signal processing technique is adopted in the developed imaging system to obtain IF signal. That is, IF signal is output by mixing the transmitted signal and the echoed signal, and it can be written as

$$s(t) = g \cdot \exp[-jnk_r(2\tau_R t - \tau_R^2)] \exp(-j2\pi f_c \tau_R),$$

where $\pi k_r \tau_R^2$ is the residual phase error (RVP) after dechirp. In general, this item can be ignored for imaging. Then, equation (3) can be simplified as

$$s(t) = g \cdot \exp[-j2\pi (k + f_c) \tau_R],$$

where $f = k + f_c$, so the above expression can be rewritten as

$$s(t) = g \cdot \exp(-j4\pi f R/c).$$

3. Range Migration Algorithm for THz FMCW Radar Imaging

Though several algorithms have been developed for THz FMCW radar imaging, RMA in the wavenumber domain is widely used due to a higher efficiency. The imaging geometry and RMA for THz FMCW radar will be introduced in this section.

The imaging geometry of the developed imaging system is presented in Figure 3. The transceiver mounted on the planar scanner is controlled to move with a grid-like manner, which will lead to a 2D rectangular synthetic aperture formation on the X'Y'O' plane which is parallel to the XOY plane.

For the convenience of expression, equation (5) is rewritten as
where \( k = 2\pi f/c \) and \( R = \sqrt{(x'-x)^2 + (y'-y)^2 + (z_0-z)^2} \) is the range between the measurement point \((x', y', z_0)\) and the scattering center \((x, y, z)\). Then, the sum of all received echoed signals at a measurement point \((x', y', z_0)\) within the imaging area is

\[
s(x', y', k) = \int_{P} g(x, y, z) e^{-j2kr} dx dy dz,
\]

where \( P \) denotes the imaging area and \( g(x, y, z) \) represents the reflection coefficient matrix of target.

Applying two-dimensional Fourier transform of the received echoed signals along the scanning direction,

\[
S(k_x, k_y, k) = \int_{P} \int \int \int g(x, y, z) e^{-j2kr} dx dy dz \cdot e^{-jk_x x'} e^{-jk_y y'} dx' dy'.
\]

where \( k_x \) and \( k_y \) represent the spatial frequencies in the \( X \)- and \( Y \)-directions and \( S_0(k_x, k_y, k) = \int e^{-j2kr} e^{-jk_x x'} e^{-jk_y y'} dx' dy' \). And \( S_0(k_x, k_y, k) \) can be solved as
\[ S_0(k_x, k_y, k_z) = e^{i \sqrt{k_x^2 + k_y^2 + k_z^2} (z_0 - z)} e^{-j k_x x} e^{-j k_y y}. \] (9)

Considering that \( k_x^2 + k_y^2 + k_z^2 = 4k^2 \), equation (8) can be rewritten as

\[ S(k_x, k_y, k_z) = \int_{\mathbb{R}^3} g(x, y, z) e^{i \sqrt{k_x^2 + k_y^2 + k_z^2} (z_0 - z)} e^{-j k_x x} e^{-j k_y y} e^{-j k_z z} dx dy dz. \] (10)

After multiplying the reference function \( e^{-i \sqrt{k_x^2 + k_y^2 + k_z^2} z_0} \), we can obtain the following expression:

\[ S_1(k_x, k_y, k_z) = \int_{\mathbb{R}^3} g(x, y, z) e^{-j k_x x} e^{-j k_y y} e^{-j k_z z} dx dy dz. \] (11)

It can be found from equation (11) that \( S_1(k_x, k_y, k_z) \) is the Fourier transform of \( g(x, y, z) \), so the reflection coefficient matrix \( g(x, y, z) \) which corresponds to the image of target can be derived by applying inverse Fourier transform. However, the measured data are not uniformly distributed in the \( k_z \) domain due to a nonlinear conversion from \( k \) to \( k_z \). Generally, the Stolt interpolation method is used to obtain a uniformly distributed data in the \( k_z \) domain. Finally, the reflection coefficient matrix \( g(x, y, z) \) can be obtained with

\[ g(x, y, z) = \text{IFFT}(k_x, k_y, k_z) \cdot \text{stolt}_{k_z \rightarrow z_0}[S(k_x, k_y, k_z) e^{i \sqrt{k_x^2 + k_y^2 + k_z^2} z_0}]. \] (12)

The THz FMCW SAR imaging algorithm based on RMA can be summarized as follows:

1. 2D Fourier transform is applied on the data collected by planar scanning to obtain wavenumber domain formulation \( S(k_x, k_y, k_z) \).
2. The reference function \( e^{-i \sqrt{k_x^2 + k_y^2 + k_z^2} z_0} \) is multiplied at the reference range \( z_0 \).
3. Stolt interpolation is performed to generate data which are uniformly distributed in the \( k_z \) domain.
4. Finally, 3D inverse Fourier transform is performed to produce the image of target.

### 4. Imaging Algorithm Based on Compressed Sensing

#### 4.1. Compressed Sensing Principle

Compressed sensing is a signal processing technique which is able to realize the recovery of a sparse signal with fewer samplers required by the Nyquist sampling theorem. In view of the advantages of compressed sensing, this technique is investigated for THz FMCW SAR imaging to reduce the requirement for data sampling and to increase the imaging speed.

Suppose \( g \) is a discrete signal with a length of \( N \) in the time domain, and it can be represented linearly by a set of orthonormal basis as

\[ g = \Psi x = \sum_{i=1}^{N} \Psi_i x_i, \] (13)

where \( \Psi = [\Psi_1, \ldots, \Psi_N] \) is the sparse transformation basis and \( x = [x_1, \ldots, x_N] \) is the weighting coefficients of \( g \) satisfying that \( x_i = \Psi_i^t g \).

It can be seen from equation (13) that \( x \) is the equivalent representation of \( g \). If there are only \( K \) nonzero elements in \( x \), then \( x \) is the \( K \)-sparse representation of signal \( g \), and the signal sparsity is \( K \).

Generally, the received THz FMCW radar signal is nonsparse in the time domain. So, it is necessary to transform the nonspare time domain signal to the sparse transform domain. Fourier transform is employed here for signal transform operations in this paper. Compressed sampling is realized with a measurement matrix \( \Phi \) which projects high-dimensional signal on the low-dimensional space:

\[ y = \Phi g = \Phi \Psi x = Ax, \] (14)

where \( y \) is the vector of measurements of the original high-dimensional signal \( g \) under a random matrix \( \Phi \), \( \Psi \) is the sparse basis matrix, and \( A = \Phi \Psi \) is the sensing matrix with a dimension of \( M \times N \) \((M \ll N)\).

The \( N \)-dimensional signal \( x \) can be recovered from the \( M \)-dimensional measurement data through signal reconstruction. And the signal reconstruction is realized by solving the \( L_0 \)-norm minimization problem expressed as

\[ \bar{x} = \arg \min \| x \|_0, \quad \text{s.t. } y = Ax. \] (15)

Though the above minimum \( L_0 \)-norm is an NP-hard problem which cannot be solved directly, an optimal solution can be realized with greedy search or convex optimization algorithms.

#### 4.2. THz FMCW Radar Imaging Algorithm Based on Compressed Sensing

Because the recovery accuracy of greedy search reconstruction algorithms like orthogonal matching pursuit (OMP) [14, 15], stage-wise orthogonal matching pursuit (StOMP) [16], regularized orthogonal matching pursuit (ROMP) [17], and compressive sampling matching pursuit (CoSaMP) [18] is poor with lower signal noise ratio (SNR), an improved smoothed \( L_0 \)-norm minimization (SL0) algorithm based on the convex optimization is presented in this paper.

For the SL0 algorithm, the objective function is defined as follows [19, 20]:

\[ \begin{align*}
\text{arg min } F_\sigma(x), \\
\text{s.t. } y = Ax, \\
\| x \|_0 = \lim_{\sigma \to 0} F_\sigma(x) = \lim_{\sigma \to 0} \sum_{i=1}^{N} F_\sigma(x_i),
\end{align*} \] (16)

where \( F_\sigma(x) \) is a smoothed function, which can be regarded as \( \| x \|_0 \) when \( \sigma \) is close to 0. It is obvious that the smoothed function \( F_\sigma(x) \) will approximate to the optimal solution by choosing a suitable \( \sigma \). And \( F_\sigma(x_i) \) is defined as...
\[ F_{\sigma}(x_i) = \frac{\exp\left(x_i^2/2\sigma^2\right) - \exp\left(-x_i^2/2\sigma^2\right)}{\exp(x_i^2/2\sigma^2) + \exp(-x_i^2/2\sigma^2)}. \]  

(17)

Compared with the Gauss smoothed function, the presented smoothed function will get a better performance in signal reconstruction as this leads to a closer approximation to \( ||x|| \).

The steepest descent algorithm is commonly applied to solve equation (16). However, it is difficult to estimate the optimal searching step in the algorithm, and this will lead to a slower convergence speed. A revised Newton method in [21] is utilized in this paper to solve the optimization problem more efficiently. The revised Newton directions is revised as

\[ d = -G^{-1}V F_{\sigma}(x), \]  

(18)

where \( V F_{\sigma}(x) = [(\partial f_{\sigma}(x_j)/\partial x_j), \ldots, (\partial f_{\sigma}(x_N)/\partial x_N)]^T \), \( G = V^T (F_{\sigma}(x)) + \epsilon_k I \), \( I \) is identity matrix, and \( \epsilon_k \) is positive to make sure that diagonal values of \( G \) are also positive. Here, \( \epsilon_k \) is set as

\[ \epsilon_k = \frac{4/\sigma^2 \left[ 3 \left( x_i^2 / \sigma^2 \right) \exp(-x_i^2 / 2\sigma^2) - \left( x_i^2 / \sigma^2 \right) \exp\left(x_i^2 / 2\sigma^2\right) \right]}{\left[ \exp(-x_i^2 / 2\sigma^2) + \exp(-x_i^2 / 2\sigma^2) \right]^3}. \]  

(19)

So, the revised Newton directions can be written as

\[ d = \left( -\frac{\sigma^2 x_1}{\sigma^2 + x_1^2}, \ldots, -\frac{\sigma^2 x_j}{\sigma^2 + x_j^2}, \ldots, -\frac{\sigma^2 x_n}{\sigma^2 + x_n^2} \right)^T. \]  

(20)

The realization steps of the presented sparse signal reconstruction algorithm based on the Newton smooth \( L_0 \)-norm (NSL0) are summarized in Table 2.

**Table 2: NSL0 algorithm.**

| Sparsity rate (%) | SLO | NSL0 |
|-------------------|-----|------|
| 10                | 7.8157 | 6.8796 |
| 20                | 11.6065 | 10.6881 |
| 30                | 17.2381 | 16.3765 |
| 40                | 24.3518 | 23.1646 |
| 50                | 32.8382 | 31.9270 |

Based on the above sparse signal reconstruction algorithm, the 3D imaging algorithm of THz FMCW SAR based on compressed sensing proposed in this paper can be summarized as follows:

1. Design a measurement matrix \( \phi \) which is able to meet the requirement for data acquisition
2. Collect THz FMCW SAR echoed signal at the corresponding position given by the designed measurement matrix to obtain measurement signal \( y \)
3. Reconstruct original signal \( \hat{g} \) from the sparse measurement data using the presented NSL0 algorithm
4. Apply 2D Fourier transform with respect to the reconstructed signal \( \hat{g} \)
5. Perform reference function multiplying (RFM)
6. Perform Stolt interpolation
7. Perform 3D inverse Fourier transform to generate the image

The proposed THz FMCW SAR imaging algorithm based on compressed sensing is shown in Figure 4.

5. Experimental Result

Simulation and measurement experiments are performed to verify the presented THz FMCW SAR imaging algorithm in this paper.

5.1. Point Targets Simulation. The THz FMCW SAR imaging model is built with MATLAB, and six-point targets are simulated for imaging. The coordinates of targets are \((0.2m, 0m, 0m), (-0.2m, 0m, 0m), (0m, 0.2m, 0m), (0m, -0.2m, 0m), (0m, 0m, 0.2m), \) and \((0m, 0m, -0.2m)\). The imaging radar system parameters used in the simulation are listed in Table 3. The measurement matrix used in the simulation is a sparse random matrix, and the sparse sampling rate is 50%.

The sparse simulated data are firstly recovered with compressed sensing. Then, the recovered signal is processed with RMA to produce a 3D image as shown in Figure 5(a). Also, the imaging results with the full data using RMA are presented in Figure 5(b) for comparison.

It can be seen from the figures that the produced 3D images are almost the same. And, it shows that the presented THz FMCW SAR imaging algorithm works well with the sparse measurement.
Figure 4: THz FMCW SAR imaging algorithm based on compressed sensing.

Table 3: Simulation parameters.

| Parameter                          | Value               |
|------------------------------------|---------------------|
| Frequency range                    | 170 GHz–220 GHz     |
| Bandwidth                          | 50 GHz              |
| Distance z₀                        | 0.5 m               |
| Scanning step along X₀-axis        | 0.001 m             |
| Scanning step along Y₀-axis        | 0.001 m             |
| Scanning points along X₀-axis      | 1000                |
| Scanning points along Y₀-axis      | 1000                |

Figure 5: Reconstructed 3D images of point targets: (a) presented algorithm in this paper; (b) RMA.
Figure 6: Targets for imaging experiments: (a) disc; (b) scissors.

Figure 7: Reconstructed 3D images of targets with RMA: (a) disc; (b) scissors.

Figure 8: Continued.
5.2. Measurement Experiment. In order to further verify the proposed 3D imaging algorithm for THz FMCW SAR, experiments are conducted with the developed THz FMCW imaging radar system. The operation frequency range of the system is 170–220 GHz. The targets to be imaged are placed on a foam column which is 0.5 m away from the planar
scanning plane, and the scanning area is 151 mm \times 151 mm. The planar scanner moves with a “stop-go-stop” manner with a scanning step of 1 mm. The collected full data are processed to reconstruct the image of target with RMA first. The reconstructed images of a disc and a pair of scissors as shown in Figure 6 are presented in Figure 7. Then, 10%, 20%, 30%, and 50% of the collected data are extracted according to the measurement matrix \( \phi \). The extracted sparse data are then processed with the proposed compressed sensing imaging algorithm. The reconstructed images under different sparsity rates are shown in Figures 8 and 9.

It can be seen from the experimental results that the reconstructed 3D image quality is poor with the 10% data sparsity rate, and it is difficult to identify the specific targets. However, the images can be reconstructed well even at 20% data sparsity rate. And a larger data will result in a better image. Also, a reconstruction error \( \varepsilon \) is introduced to evaluate the quality of the images reconstructed with different reconstruction algorithms:

\[
\varepsilon = \frac{\sqrt{\sum_{i=1}^{n} \left| g_i'(x, y, z) - g_i(x, y, z) \right|^2}}{\sqrt{\sum_{i=1}^{n} |g_i(x, y, z)|^2}} / n^2,
\]

where \( g_i'(x, y, z) \) is the reconstructed signal and \( g_i(x, y, z) \) denotes the original signal. A larger \( \varepsilon \) denotes a significant deviation of the reconstructed signal from the original signal and thus means a poorer performance of the reconstruction algorithm. The reconstruction error comparisons between SL0 and NSL0 under different sparsity rates are listed in Table 4.

Also, the calculation time of the algorithms is presented in Table 5. The CPU is Intel Core i5-4210 M @ 2.6 GHz, and the memory is 8 GB.

The above results show that the presented NSL0 reconstruction algorithm has a smaller error and a fast calculation speed compared with the SL0 reconstruction algorithm. This is contributed by Newton’s method in the NSL0 algorithm.

### 6. Conclusions

An algorithm for THz FMCW SAR imaging based on compressed sensing is investigated in this paper. The developed 220 GHz FMCW imaging radar system is introduced, and the signal model is built firstly. RMA for the developed THz FMCW SAR is then derived. Compressed sensing is described, and the NSL0 reconstruction algorithm is presented to reconstruct signal with sparse samples. And the algorithm based on compressed sensing for the developed THz FMCW SAR is summarized. Experiments are performed to verify the presented imaging algorithms. The experimental results show that it is able to reconstruct the image well even at the sparsity rate of 20%. The presented 3D imaging algorithm for the THz FMCW imaging radar system can improve the imaging efficiency by reducing the requirements for spatial data acquisition.

The developed 220 GHz FMCW SAR imaging system has been used for nondestructive testing of composite materials in aerospace and critical structural applications. As only a single transceiver is integrated in the system, it must employ a grid-like mechanical scanning to cover an area and results in a high time cost. The imaging system can be upgraded to multiple transceivers which will have a faster imaging speed. The proposed compressed sensing image reconstruction algorithm can be also applied for sparse transceiver array configuration which is able to achieve a lower imaging system cost by reducing THz transceivers.

### Data Availability

The data used to support this study are included within this articles as tables. If there is a need for any other information, the corresponding author may be contacted by e-mail.

### Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

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