Neutrino Superbeam Scenarios at the Peak

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We discuss options for U.S. long baseline neutrino experiments using upgraded conventional neutrino beams, assuming \( L/E \) is chosen to be near the peak of the leading oscillation. We find that for \( L = 1290 \text{ km} \) (FNAL–Homestake) or \( 1770 \text{ km} \) (FNAL–Carlsbad, or BNL–Soudan) it is possible to simultaneously have good \( \sin^2 2\theta_{13} \) reach and \( \text{sgn}(\delta m^2_{31}) \) determination, and possibly sizeable \( \tau \) rates and some \( \delta \) sensitivity.

In this report we discuss possible--neutrino scenarios for long baseline neutrino experiments using upgraded conventional neutrino beams (superbeams). In each case we examine their ability to measure \( \nu_\mu \rightarrow \nu_e \) and \( \nu_\mu \rightarrow \nu_\tau \) appearance, discover CP violation, and to determine the sign of the leading \( \delta m^2 \). Details of our calculations can be found in Ref. [1]. For the \( \nu_\mu \rightarrow \nu_\tau \) oscillation probability we use the approximate analytic expressions of Ref. [2],[3], which are particularly helpful in determining the general properties described below. We emphasize that many other beam design and source–detector configurations are possible; the scenarios discussed here illustrate some of the capabilities of such facilities.

We choose five distances that could be appropriate for likely proton driver and detector sites (see Table I): 350 km (BNL–Cornell, or similar to the 295 km of JHF–SK), 730 km (FNAL–Soudan or CERN–Gran Sasso), 1290 km (FNAL–Homestake, or similar to the 1200 km of JHF–Seoul), 1770 km (FNAL–Carlsbad, or similar to the 1720 km of BNL–Soudan), and 2900 km (FNAL–SLAC, or similar to the 2920 km of BNL–Carlsbad). The latter distance would also be similar to FNAL–San Jacinto (2640 km) or BNL–Homestake (2540 km).

For each \( L \), we choose \( \langle E_\nu \rangle \) such that \( \Delta = 1.27 \delta m^2_{31} \text{ (eV)}^2 L \text{ (km)}/\langle E_\nu \rangle \text{ (GeV)} = \pi/2 \), i.e., \( L/E_\nu = 353 \text{ km}/\text{GeV} \) for \( \delta m^2_{31} = 3.5 \times 10^{-3} \text{ eV}^2 \). This has three important advantages: (i) the \( \nu_\mu \rightarrow \nu_\tau \) oscillation (which has only small matter effects) is maximal, (ii) the \( \nu_\mu \rightarrow \nu_e \) oscillation is nearly maximal, even when matter effects are taken into account [1], and (iii) in the relevant limits that \( \theta_{13} \) and \( \delta m^2_{21}/\delta m^2_{31} \) are small, the \( \delta \) dependence is pure \( \sin \delta \), even in the presence of matter [1]. The latter fact implies that there is no \( \delta–\theta_{13} \) ambiguity for a given \( \text{sgn}(\delta m^2_{31}) \). There is a \( \delta–(\pi–\delta) \) ambiguity, but it does not confuse a CP violating (CPV) solution with a CP conserving (CPC) one. However, for small enough \( \theta_{13} \) and/or \( L \), there is a \( \delta, \theta_{13}–\text{sgn}(\delta m^2_{31}) \) ambiguity, which sometimes can confuse CPV and CPC solutions; when combined with the \( \delta–(\pi–\delta) \) ambiguity it results in an overall four–fold ambiguity in parameters in these cases [1]. Thus distinguishing the sign of \( \delta m^2_{31} \) may be essential for determining the existence of CPV.

We assume a narrow band beam (NBB) with flux \( 4 \times 10^{11}/\text{m}^2/\text{yr} \) at \( L = 730 \text{ km} \) (and proportional to \( 1/L^2 \)), which would be about 1/5 of the flux (to represent the flux loss in making a NBB) of an upgraded NuMI ME beam with a 1.6 MW proton driver. The NBB has two advantages: (i) the lack of a significant high–energy tail reduces backgrounds, and (ii) nearly all of the neutrinos will be at the same beam with a 1.6 MW proton driver. The NBB has two advantages: (i) the lack of a significant high–energy tail reduces backgrounds, and (ii) nearly all of the neutrinos will be at the same beam with a 1.6 MW proton driver. The NBB has two advantages: (i) the lack of a significant high–energy tail reduces backgrounds, and (ii) nearly all of the neutrinos will be at the same beam with a 1.6 MW proton driver.

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We assume an effective 70 kt-yr of data accumulation for detecting \( \nu_e \)’s, which could be achieved by 2 years of running with a 70 kt liquid Argon detector [2] at 50% efficiency [2]. For \( \nu_\tau \) detection we assume 3.3 kt-yr (2 years with a 5 kt detector at 33% efficiency). For \( \nu_\bar{\nu} \)’s, we assume approximately 6–12 years of running (a factor of two longer to account for the lower \( \bar{\nu} \) cross section and another factor of 1.5–3 longer, depending on \( E_\nu \), to account for the reduced \( \bar{\nu} \) flux in the beam). Thus in the absence of matter and/or CPV the number of \( \nu \) and \( \bar{\nu} \) events would be the same. We assume a \( \nu_e \) background of 0.4% of the unoscillated CC signal, and a fractional uncertainty of the background of 10%.

We expect \( \delta m^2_{21} \) to be measured to 10% accuracy at KamLAND [2], and \( \delta m^2_{31} \) to be measured to about the same accuracy by K2K, MINOS, and ICANOE, and OPERA. Since \( E_\nu \) is chosen to be at the peak of the leading oscillation, the choice of \( E_\nu \) depends critically on the value of \( \delta m^2_{31} \); also, the size of the CPV and the potential

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TABLE I. Baseline distances for some detector sites (shown in parentheses) for neutrino beams from FNAL, BNL, JHF, and CERN.

| Beam source | FNAL | BNL | JHF | CERN |
|-------------|------|-----|-----|------|
| 730 (Soudan) | 350 (Cornell) | 295 (Super-K) | 730 (Gran Sasso) |
| 1200 (Homestake) | 1200 (Seattle) |
| 1700 (Carlsbad) | 1700 (Soudan) |
| 2640 (San Jacinto) | 2540 (Homestake) |
| 2900 (SLAC) | 2920 (Carlsbad) |

for confusion between $\delta m_{31}^2 > 0$ and $\delta m_{31}^2 < 0$ increases with increasing $\delta m_{31}^2$. Our results for $\delta m_{31}^2 > 0$ with $\theta_{23} = \pi/4$ are presented in Table II (for two values of $\delta m_{31}^2 = 5 \times 10^{-5}$ eV$^2$ (the value preferred from recent analyses of solar neutrino data) and $\delta m_{31}^2 = 10^{-6}$ eV$^2$; the corresponding results for $\delta m_{31}^2 < 0$ are found by interchanging $(N_e) \leftrightarrow (\bar{N}_e)$ and $(\nu_\mu \rightarrow \nu_e) \leftrightarrow (\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$. For each value of $\delta m_{31}^2$ we show results for three values of $\delta m_{23}^2$ that cover the range inferred from Super–K atmospheric neutrino data. Given in the table are (i) the numbers of $e$ and $\bar{e}$ events (for $\sin^2 2\theta_{13} = 0.01$ and averaged over $\delta$), background $e$ events ($B_e$, assumed the same for $e$ and $\bar{e}$), and $\tau$ events, (ii) the $\sin^2 2\theta_{13}$ reach at $3\sigma$ for $\nu_\mu \rightarrow \nu_e$ and $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ appearance, and the minimum $\sin^2 2\theta_{13}$ for which $\text{sgn}(\delta m_{31}^2)$ can be determined, and (iii) the smallest value of the CP phase $\delta$ that can be distinguished from $\delta = 0, \pi$ at the $3\sigma$ level for $\sin^2 2\theta_{13} = 0.01$ (not accounting for a possible $\text{sgn}(\delta m_{31}^2)$ ambiguity). The $\sin^2 2\theta_{13}$ reaches and $\delta$ sensitivity include the effects of statistical and systematic experimental uncertainties. The $e$ and $\bar{e}$ event rates approximately scale with $\sin^2 2\theta_{13}$. Results for JHF–SK running for 5 years with neutrinos only $\nu_\mu$, using a $2^\circ$ off axis beam, are also shown in the table.

TABLE II. Scenarios with $\delta m_{31}^2 > 0$ (2 years $\nu$, 6–12 years $\bar{\nu}$); the last entry in the table shows the results for JHF–SK [11] (5 years, $\nu$ only), $\theta_{23} = \pi/4$ is assumed.

| Scenario | $\delta m_{31}^2$ (eV$^2$) | $\delta m_{21}^2$ (eV$^2$) | $L$ (km) | $E$ (GeV) | $\langle N_e \rangle$ | $\langle \bar{N}_e \rangle$ | $B_e$ | $N_e$ | $\sin^2 2\theta_{13}$ reach at 3$\sigma$ | $\text{sgn}(\delta m_{31}^2)$ | $|\delta| (\degree)$ at $3\sigma$ | $\sin^2 2\theta_{13} = 0.01$ |
|----------|----------------|-----------------|--------|--------|----------------|----------------|------|------|----------------|----------------|----------------|----------------|
| $5 \times 10^{-5}$ | $2 \times 10^{-6}$ | 350 | 0.57 | 180 | 148 | 116 | - | 0.0020 | 0.0025 | - | 26 |
| 730 | 1.18 | 95 | 63 | 56 | - | 0.0026 | 0.0042 | 0.10 | - | 35 |
| 1290 | 2.09 | 64 | 27 | 32 | - | 0.0031 | 0.0082 | 0.036 | - | 49 |
| 1770 | 2.86 | 53 | 15 | 23 | - | 0.0033 | 0.014 | 0.020 | - | 67 |
| 2900 | 4.70 | 39 | 4 | 14 | 10 | 0.0038 | 0.055 | 0.011 | - | 83 |
| $3.5 \times 10^{-5}$ | | 350 | 0.57 | 294 | 217 | 204 | - | 0.0024 | 0.0029 | - | 39 |
| 730 | 2.07 | 156 | 100 | 97 | - | 0.0026 | 0.0042 | 0.050 | - | 52 |
| 1290 | 3.65 | 106 | 42 | 55 | 14 | 0.0027 | 0.0073 | 0.015 | - | 93 |
| 1770 | 5.01 | 88 | 22 | 40 | 36 | 0.0028 | 0.012 | 0.0093 | - | 30 |
| 2900 | 8.22 | 67 | 5 | 25 | 51 | 0.0029 | 0.043 | 0.0057 | - | 53 |
| $5 \times 10^{-5}$ | | 350 | 1.41 | 412 | 331 | 289 | - | 0.0024 | 0.0030 | 0.009 | 54 |
| 730 | 2.96 | 219 | 139 | 139 | - | 0.0025 | 0.0040 | 0.028 | - | 80 |
| 1290 | 5.21 | 150 | 57 | 79 | 77 | 0.0025 | 0.0066 | 0.0095 | - | 90 |
| 1770 | 7.16 | 125 | 30 | 58 | 100 | 0.0025 | 0.011 | 0.0061 | - | 96 |
| 2900 | 11.74 | 95 | 7 | 35 | 102 | 0.0025 | 0.038 | 0.0044 | - | 110 |
| $10^{-4}$ | $2 \times 10^{-4}$ | 350 | 0.57 | 233 | 261 | 116 | - | 0 | 14 |
| 730 | 1.18 | 120 | 88 | 56 | - | 0 | - | 18 |
| 1290 | 2.09 | 78 | 41 | 32 | - | 0.0007 | 0.0019 | 0.10 | - | 24 |
| 1770 | 2.86 | 62 | 24 | 23 | - | 0.0014 | 0.0059 | 0.055 | - | 30 |
| 2900 | 4.70 | 44 | 9 | 14 | 10 | 0.0023 | 0.036 | 0.023 | - | 51 |
| $3.5 \times 10^{-5}$ | | 350 | 0.99 | 324 | 268 | 204 | - | 0.0013 | 0.0016 | - | 19 |
| 730 | 2.07 | 170 | 114 | 97 | - | 0.0017 | 0.0026 | - | - | 24 |
| 1290 | 3.65 | 114 | 50 | 55 | 14 | 0.0020 | 0.0065 | 0.040 | - | 32 |
| 1770 | 5.01 | 94 | 28 | 40 | 36 | 0.0022 | 0.0092 | 0.021 | - | 40 |
| 2900 | 8.22 | 69 | 8 | 25 | 51 | 0.0025 | 0.037 | 0.010 | - | 76 |
| $5 \times 10^{-5}$ | | 350 | 1.41 | 433 | 353 | 289 | - | 0.0018 | 0.0023 | - | 25 |
| 730 | 2.96 | 229 | 149 | 139 | - | 0.0020 | 0.0032 | 0.081 | 31 |
| 1290 | 5.21 | 148 | 55 | 79 | 77 | 0.0021 | 0.0056 | 0.022 | - | 40 |
| 1770 | 7.16 | 129 | 34 | 58 | 100 | 0.0022 | 0.0092 | 0.012 | - | 50 |
| 2900 | 11.74 | 96 | 9 | 35 | 102 | 0.0023 | 0.033 | 0.0063 | - | 62 |
| $3 \times 10^{-5}$ | | 295 | 0.7 | 12 | 22 | - | 0.016 | - | - | - | - | - | - |
which in some cases could include a CPV/CPC confusion; also, $E_\nu$ is generally below the $\tau$ threshold.

If $\delta m_{21}^2$ is at the low end of its expected range, CPV can only be tested at shorter $L$, with the loss of the $\tau$ signal and sgn($\delta m_{21}^2$) determination sensitivity, and potential CPV/CPC confusion due to sgn($\delta m_{31}^2$) (the four–fold ambiguity mentioned above). Longer $L$ (such as $L = 2900$ km) could potentially do everything except for CPV, although if $\delta m_{31}^2$ is too low $\tau$‘s are not observable. If $\delta m_{31}^2 \simeq 2 \times 10^{-3}$ eV$^2$ and a large $\tau$ signal is desired, then the strategy outlined in this report will not work; $E_\nu$ must be increased, which would force $L/E_\nu$ to be off the peak of the oscillation.

For $L = 1290$ or $1770$ km it is possible to simultaneously have good $\sin^2 2\theta_{13}$ reach and sgn($\delta m_{31}^2$) determination, and possibly sizeable $\tau$ rates and some $\delta$ sensitivity if both $\delta m_{21}^2$ and $\delta m_{31}^2$ are at the high end of their expected ranges (see Table II); $L = 1770$ km is probably preferred in these cases due to its larger $\tau$ rate and better sgn($\delta m_{31}^2$) determination.

We note that while a larger $\delta m_{21}^2$ in principle improves the CPV sensitivity, it also makes a sgn($\delta m_{31}^2$) ambiguity more likely, leading to an overall four–fold ambiguity. Even if sgn($\delta m_{31}^2$) is determined, measurements on the oscillation peak will leave a two–fold ambiguity between $\delta$ and $\pi - \delta$. Measurements at different $L$ and/or $E_\nu$ will be required to resolve these ambiguities.

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