Bio-inspired Polarization Event Camera

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1 Abstract

The stomatopod (mantis shrimp) visual system has recently provided a blueprint for the design of paradigm-shifting polarization and multispectral imaging sensors, enabling solutions to challenging medical and remote sensing problems. However, these bioinspired sensors lack the high dynamic range (HDR) and asynchronous polarization vision capabilities of the stomatopod visual system, limiting temporal resolution to ∼12 ms and dynamic range to ∼72 dB. Here we present a novel stomatopod-inspired polarization camera which mimics the sustained and transient biological visual pathways to save power and sample data beyond the maximum Nyquist frame rate. This bio-inspired sensor simultaneously captures both synchronous intensity frames and asynchronous polarization brightness change information with sub-millisecond latencies over a million-fold range of illumination. Our PDAVIS camera is comprised of 346x260 pixels, organized in 2-by-2 macropixels, which filter the incoming light with four linear polarization filters offset by 45°. Polarization information is reconstructed using both low cost and latency event-based algorithms and more accurate but slower deep neural networks. Our sensor is used to image HDR polarization scenes which vary at high speeds and to observe dynamical properties of single collagen fibers in bovine tendon under rapid cyclical loads.

2 Main

Visual information is encoded in light by intensity, color, and polarization. This information is sensed by biological eyes and artificial cameras which each have been optimized by evolution driven by maximum fitness. Eyes have evolved to support visually guided behavior for the benefit of survival, while digital cameras have mainly evolved to supply consumer demand for high-resolution photography. These different evolutionary paths have created very different visual systems. Existing spectral and polarization digital cameras use synchronous and generally redundant frames with linear photo response. By contrast, eyes are asynchronous, have a compressed nonlinear response, and their output is sparse and highly informative.

The mantis shrimp visual system (Fig. 1a) is considered one of the most sophisticated visual systems in nature. It is sensitive to more than 12 spectral, 4 linear, and 2 circular polarization channels. Its photosensitive microvilli have a logarithmic HDR response to incident light. Sensitivity to linearly polarized light is in part expressed in the dorsal and ventral parts of the ommatidia, where individual photoreceptors are comprised of orthogonal sets of microvilli sensitive to orthogonal polarization states. The dorsal/ventral views largely overlap, and since the dorsal and ventral microvilli are offset by 45°, four linear polarization states offset by 45° are captured by the eye. The logarithmic photo responses of the microvilli enable high dynamic range polarization sensing capabilities, while their asynchronous response to temporally varying brightness greatly reduces the visual information that is transmitted to
Figure 1: Overview of our bio-inspired polarization vision sensor. a, Polarization vision in the mantis shrimp eye (left) is in part enabled by two sets of orthogonal microvilli located in the dorsal and ventral hemisphere (center), capturing total of 4 linear polarization states offset by 45 degrees (right). This polarization sensitivity paired with logarithmic photoreceptors that output only brightness change enable the mantis shrimp to be effective predator in the shallow coral reefs. b, The PDAVIS polarization event camera (left), effectively mimics the mantis shrimp eye by integrating an array of pixelated polarization filters offset by 45 degrees (center, angle indicated by false colors) with a vision sensor that provides both sustained pathway frames and transient pathway log-scale brightness change events (right) (see Supplementary Material 1). c, A rectangular rotating linear polarizer (left) generates a stream of brightness change events from the four subpixels in the PDAVIS macropixels that see the polarizer (center). A temporal filter approximates the temporal derivative from the four individual pixels and then computes the AoP. The result is a stream of AoP events with low latency (right) (see Supplementary Material 2). d, A polarization filter wheel is rotated in front of PDAVIS, which produces frames and events (left) represented in false colors shown in (c). A DNN (center-left) reconstructs DoLP (center-right) and AoP (right) from the brightness change events at a higher rate than the cameras maximum frame rate (see Supplementary Material 2).
their brain for further processing. It is believed that mantis shrimp use polarization to discriminate short-range prey, to select a mating partner, and to orient during short-range navigation using celestial polarization patterns.

Our work capitalizes on the development of bioinspired neuromorphic vision sensors, which have enabled higher dynamic range and lower latency machine vision. Inspired by the ommatidia of mantis shrimp, individual PDAVIS subpixel circuits are each overlaid with one of four pixelated linear polarization filters (Fig. 1b). The PDAVIS takes inspiration from biology by saving energy by partitioning the perception of fine detail and fast motion into sustained and transient pathways. It provides a relatively low frequency synchronous readout of frames like conventional cameras (the “sustained” pathway), and it concurrently outputs a high frequency stream of asynchronous brightness change events (the “transient” pathway). Each event represents a signed log intensity change. Pixels that see more brightness change generate more events, and the events have sub-millisecond temporal resolution driven by the dynamics of the scene. The events enable reconstructing the absolute intensity between the synchronous frame intensity samples.

3 Reconstructing Polarization Information

Polarization is encoded in the relative responses of the subpixels with the 4 linear polarizers offset by 45°. Absolute intensity is encoded in the sum of crossed polarization subpixel outputs. For a direct comparison with a state-of-the-art commercially available polarization imaging sensor (Sony IMX250), we processed the PDAVIS output to extract Angle of Polarization (AoP), i.e., the predominant axis of oscillation as light propagates in time and space, and Degree of Linear Polarization (DoLP), i.e., the amount of linearly polarized in the incident light. We studied three related algorithms: an economical algorithm processing only events, an economical Complementary Filter (CF) algorithm which fuses frames and events, and an expensive Deep Neural Network (DNN) that takes events as input (see Methods, Supplementary Material 2 and Supplementary Table 2). We did four sets of experiments.

First, we assessed the ability to reconstruct the time-varying AoP of fully linearly polarized light (with DoLP=1) by rotating a linear polarizer at constant speeds (Fig. 2, Supplementary Video 1). At low rotation speeds of less than 60 RPM, the AoP reconstruction error from both sensors is less than 5°, with the Sony sensor having the lowest reconstruction error. The reconstructed DoLP is nearly 1 from both sensors, as expected. Since Sony’s polarization sensor is fabricated in an optimized semiconductor fab, the mismatches in both the optical properties of the pixelated polarization filters and electrical properties of the photodiodes and read-out circuits are minimal, resulting in high accuracy in the reconstructed polarization information for slow rotation rate. Our PDAVIS prototype has larger mismatches between the optical properties of the pixelated filters as well as read-out electronics resulting in larger error at low frequency, which can be mitigated by calibration. However, when the linear polarizer is rotated above ~100 RPM, the Sony and PDAVIS frames start aliasing and motion blurring (Fig. 2), which decreases the estimated DoLP and increases the AoP error. The PDAVIS events maintain precise timing information and the reconstructions using events have AoP and DoLP error less than 10° all the way to 1000 RPM.

The second experiment (Fig. 3, Supplementary Video 2) assessed the ability to measure time-varying DoLP while DoLP and AoP both vary with time. We combined a rotating linear polarizer with a fixed Quarter Wave Plate (QWP). Fig. 3a shows how much the DoLP error increases as a function of the speed of the QWP, compared to 30 RPM. For visual comparison, each method is defined to have zero “change of error” at the lowest frequency. Fig. 3b shows the absolute DoLP measured by each method for 30 and 1000 RPM. At low RPM, the Sony camera makes the most accurate estimate of DoLP. When the QWP is rotated at higher speeds, the frames from both cameras become aliased and motion blurred, resulting in a large error increase of over 50% in the Sony DoLP; at 1000 RPM, the Sony frames are hopelessly blurred and aliased (Fig. 3b, Sony (frames)). However, the CF method fuses the PDAVIS events with its 20 FPS frames, clearly improving the reconstruction in comparison with the 50 FPS Sony (Fig. 3b, PDAVIS CF). Finally, using only the PDAVIS events with the DNN method keeps the growth in reconstruction error below 8% all the way to 1000 RPM (Fig. 3c, PDAVIS DNN). Fig. 3c shows the statistics of the events. At 30 RPM, the distribution of interevent time intervals (lower histogram) shows that the events are widely spaced because the brightness changes are slow. At 1000 RPM, the distribution moves to much shorter event intervals, down to less than 1 ms. The event rate (Fig. 3, upper plot) is directly proportional to RPM. The insets of the event rate plot show events from one pixel; the structure of ON and OFF events is similar for 30 RPM and 1000 RPM, but speeds up by a factor of 30. This low latency asynchronous PDAVIS output allows the measurement of fast brightness changes, which occur...
Figure 2: Comparison of frame-based and event-based AoP and DoLP reconstruction accuracy at various rotational speeds. Input is image of fully linearly polarized light from a rotating linear polarizer. 

(a) Mean absolute error (MAE) of AoP reconstruction for the various methods averaged over 12x12 Region of Interest (ROI) centered on the polarizer. (see Supplementary Material 2). PDAVIS and Sony frame rates are shown in plots and both exposure durations were fixed to 20 ms. The frames methods use only synchronous intensity frames. The CF method fuses 20 FPS frames and events using a method adapted from [2]. The events method is illustrated in Fig. 1c. The DNN method uses only events together with the convolutional recurrent neural network [9].

(b) DoLP reconstructions. Both CF or DNN methods show that using events allows reconstructing DoLP well beyond the limiting Nyquist frequency of the frame sampling. Inset plots the event rate per pixel within the polarizer ROI versus RPM; the event rate outside ROI is < 1 Hz after denoising.

(c) Reconstruction of the AoP from a 100 pixel ROI using various methods. The frame based Sony and PDAVIS reconstructions are severely aliased at 1000 RPM, which is not true for any of the PDAVIS methods using events.
much more rapidly than the fixed frame rate; the PDAVIS events sample as needed, up to more than 1 kHz in this experiment.

![Figure 3: Comparison of frame-based and event-based reconstruction of DoLP with various rotation speeds of a QWP.](image)

Each cycle of QWP rotation produces four cycles of DoLP. a Growth of the mean absolute error of DoLP reconstruction with RPM. The Sony has only synchronous intensity frames (see Supplementary Material 2.1). The CF method fuses PDAVIS frames and events (see Supplementary Material 2.3). The DNN method uses only events (see Supplementary Material 2.4). b Reconstruction of the absolute DoLP from a 100 pixel ROI using various methods. The frame based Sony reconstruction is most accurate at low frequency but is severely aliased at 1000 RPM, which is not true for any of the PDAVIS methods using events. c Statistics of events. Upper plot is event rate versus QWP RPM. Insets show actual ON and OFF events from a subpixel in response to the sinusoidal intensity variation. Lower plot shows histograms of the time between two consecutive events for the two rotational speeds of the QWP.

The third experiment (Fig. 4, Supplementary Videos 3 and 4) compares the PDAVIS and Sony dynamic range. We imaged set of polarization filters offset by 30° rotating at 200 RPM (5 rev/s) under high contrast 2000:1 lighting, such as commonly encountered in remote sensing of natural environments. The Sony camera exposure is set to 20 ms to capture the darker part of the scene without underexposing it, which overexposes and saturates the brighter part, preventing AoP measurement. The large motion blur is visible in the I0 image and incorrect AoP in the blurred regions. The PDAVIS can measure the AoP in both lighting conditions. Even though the PDAVIS frame is also motion blurred, all event-based methods produce sharp images.

The fourth experiment (Fig. 4, Supplementary Video 5) shows a potential medical imaging application of the PDAVIS (see Methods and Supplementary Material 3). We imaged the dynamics of a bovine tendon subjected to cyclical stress, such that its birefringent properties are time varying. As circularly polarized light transmits through the tendon, it becomes elliptically polarized and the DoLP provides an indirect measurement of the birefringent properties, assuming minimal scattering. Using high optical magnification, we can observe strain patterns over time of the individual collagen fibers that comprise the tendon. Due to the high optical magnification and rapid movement of the collagen fibers, preventing aliasing would require a frame rate that is a large multiple of the cycle rate. By contrast, DNN reconstruction of the DoLP (using only events) provides measurement of the dynamic properties of the individual collagen fibers at higher frequency than the maximum frame rate.
Figure 4: Applications of PDAVIS for remote sensing and scientific imaging. a Images of a rotating fan polarizer under HDR illumination captured by the PDAVIS and Sony's camera using various reconstruction methods (see Supplementary Material 2). The fan is constructed from triangular linear polarizers arranged with 30° AoP spacing. The illumination ratio between bright and dark parts is 2000 and the rotation speed is 200 RPM. The I₀ images show reconstructed monochromatic intensity from pixels with 0 degree pixelated polarization filters of Fig. 1. The weakly-polarized regions in the AoP images are masked out using the measured DoLP. b Imaging a tendon that is periodically stretched at 1 Hz and 10 Hz. The images (upper half) show a single frame (left), an event time window (center) and the corresponding DoLP reconstruction result (right) using the DNN method (see Supplementary Material 3 and Supplementary Material 2). The event time window is rendered from a fixed time interval where ON (white) and OFF (black) events are accumulated to the starting gray image. The DNN input is 3D event tensors (the frames are not used) that have a duration of 50 ms or 10 ms, resulting in output at 20 or 100 FPS for 1 Hz and 10 Hz respectively. The traces (lower half) compare the DNN and frame-based reconstructed DoLP, averaged over the ROI indicated in the DoLP image (upper right). With 1 Hz stretching (left), both methods yield similar results. With 10 Hz stretching (right), the DNN reconstructs the DoLP while the 20 FPS frame-based reconstruction is severely aliased.
4 Discussion

Airborne, underwater, and space-based applications can require high temporal resolution and HDR, together with spectral and polarization sensitivity. All of these requirements increase the data rate, but the bioinspired sparse data streams and local gain control of event cameras enables near-sensor processing with low latency and a small computational footprint together with HDR. To compare PDAVIS with state-of-the-art polarization sensors, we developed novel event-driven reconstruction algorithms and compared their angle and degree of polarization reconstruction abilities to the frame-based camera reconstruction. The pure event-driven algorithm is the most economical, but it cannot reconstruct the degree of linear polarization, which requires an estimate of the absolute intensity which the event stream does not provide. The CF helps to overcome this limitation by fusing the event stream with periodically captured frames while only slightly increasing the computational cost. The DNN provides the most accurate reconstruction, but requires a power hungry and expensive GPU for real time operation, which may not be affordable in a remote environment close to the sensor or with minimum latency. A limitation of the PDAVIS is with dense scenes, which can saturate the event output capacity, causing event loss. In these situations, a conventional frame-based polarization camera could be better suited. By adopting a bioinspired combination of sustained and transient pathway, the PDAVIS bridges a gap between the limited temporal and dynamic range of conventional frame-based polarization cameras and complex solid state imagers or streak cameras that can record short sequences at $>10^7$ FPS. This gap is normally filled by high frame rate cameras that consume a lot of power and demand bright lighting for the short exposure times. The PDAVIS enables continuous AoP and DoLP measurement with high contrast illumination at frequencies several times the Nyquist rate of frame-based image sensors. The PDAVIS event output triggers data acquisition and processing only when needed making it ideally matched with the increasing development of activation-sparsity aware neural accelerators.

5 Methods

The PDAVIS Polarization Filter Array (PFA) is fabricated on a quartz wafer using interference lithography and reactive ion etching. Reactive ion etching transfers the photoresist pattern to the silicon dioxide, which serves as a hard mask for etching the underlying aluminum. The filter array is then laser cut to match the total size of the pixel array. The individual polarization filters are comprised of aluminum nanowires with 70 nm width, 70 nm spacing, and 150 nm height, and have extinction ratio of 40 at 500 nm incident light (see Methods, Supplementary Material 1, and Supplementary Figs. S3 and S4). The PFA and pixel array are aligned using a 6-DOF positioning stage and are bonded using ultraviolet-curing optical adhesive. (see Supplementary Table 1).

A custom PCB hosts the PDAVIS chip and streams data (frames and events) to the host computer (see Supplementary Material 1.1 and Supplementary Fig. S1). To recover and reconstruct information about AoP and DoLP we compared 4 different PDAVIS methods (for an overview see Supplementary Table 2 and Supplementary Material 2). It also enabled a comparison with Sony’s camera (see Supplementary Material 3 and Fig. S6). For Fig. 4b, we sectioned bovine tendons and mounted them on a custom-built stage to enable cyclical loading, and imaged them with a microscope objective (see Supplementary Material 3).

6 Data availability

The data that support the findings of this study are available within the article and its Supplementary Information. Raw data collected from the sensors are available upon request from V.G. or T.D.

7 Code availability

Software code and data used to generate polarization data are available online. The link will be made available once the paper is accepted for publication.
8 Funding

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10 Author Contributions

T.D. and V.G. conceived the idea and supervised the project. G.H. and V.G. aligned and bonded the polarization filter arrays to the DAVIS sensors. DAVIS sensor was developed by T.D lab. Measurements were performed by D.J., Y.C., and J.H. Complementary filter was developed by T.D., G.H. and D.J. DNN data analysis was performed by J.H and Y.C. G.H., D.J., T.D., and M.B.M developed the event-based reconstruction algorithm. All authors contributed to the data analysis and writing of the paper.

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Supplementary Materials

- **Supplementary Material 1** provides details of the Polarization Dynamic and Active pixel VIision Sensor (PDAVIS) pixel circuit, characterization setup, Polarization Filter Array (PFA) assembly, and specifications of the PDAVIS and Sony cameras.

- **Supplementary Material 2** provides details of PDAVIS algorithms for reconstructing polarization.

- **Supplementary Material 3** describes the setup of the bovine tendon experiment.

- **Supplementary Video 1**: The video shows both the frame and event based polarization reconstruction when a linear polarization filter is rotated in front of the PDAVIS camera. The top half of the video represents data acquired from the PDAVIS frames and the bottom half corresponds to event based reconstruction using complementary filter. The left half of the video depicts the intensity data from the four pixelated polarization filters. The right half of the video depicts the reconstructed angle of polarization. It can be observed that the frame based reconstruction (top right) updates Angle of Polarization (AoP) information at much slower speed compared to the event based reconstruction (bottom right). This video demonstrates the aliasing problems associated with frame based polarization imaging.

- **Supplementary Video 2**: The video shows both the frame and event based polarization reconstruction when a Quarter Wave Plate (QWP) filter is rotated in front of the PDAVIS camera. The top half of the video represents data acquired from the PDAVIS frames and the bottom half corresponds to event based reconstruction using the complementary filter. The left half of the video depicts the intensity data from the four pixelated polarization filters. The right half of the video depicts the reconstructed Degree of Linear Polarization (DoLP). It can be observed that the frame based (top right) updates DoLP information at much slower speed compared to the event based reconstruction (bottom right). This video demonstrates the aliasing problems associated with frame based polarization imaging.

- **Supplementary Video 3**: The video shows a high dynamic range scene comprised of six linear polarization filters rotating at ~105 RPM. The frame based data from both Sony and PDAVIS cannot fathfully reconstruct the AoP across the entire scene due to the limited dynamic range. The event based reconstruction methods leverage the high dynamic range capabilities of the PDAVIS and reconstruct AoP information across the entire scene. Furthermore, slight motion blur can be observed in both intensity and AoP images in the Sony sensor.

- **Supplementary Video 4**: The video shows motion blur problems associated with frame based polarization sensor. The filter wheel is rotated at ~1000 RPM (16.7 rev/s), causing severe motion blur in the Sony polarization sensor. Due to the "on-demand" imaging capability provided by events in the PDAVIS, motion blur in this experiment is non existent.

- **Supplementary Video 5**: Imaging single fibers of a bovine tendon under cyclical load of 1 Hz and 10 Hz. The frame based method can accurately monitor the changes of stress in single tendon fibers based on the AoP information. However, at 10 Hz cyclical load this information is severely aliased. Event based reconstruction provides updates only at the location of the fibers and provides accurate stress information at the 10 Hz cyclical load.
Supplementary Material 1  PDAVIS camera

Supplementary Material 1.1  PDAVIS chip

The DAVIS chips used to build the PDAVIS cameras were fabricated by Towerjazz Semiconductors in their Fab 2 (Migdal HaEmek, Israel), a 180nm 6-metal CMOS Image Sensor (CIS) process with optimized buried photodiodes, antireflection coating, and customized microlenses for large pixels. The chips are packaged in a ceramic PGA package with a taped glass lid, which we remove for PFA assembly.

Fig. S1 shows the PDAVIS pixel circuit. The design is based on the Dynamic Vision Sensor (DVS) and the Dynamic and Active pixel Vision Sensor (DAVIS) with improvements described in Taverni et al. [0].

Figure S1: DAVIS pixel circuit and operating principle. The sensor generates asynchronous brightness change ON and OFF DVS events and Active Pixel Sensor (APS) intensity samples.

For the DVS brightness change events, the logarithmic photoreceptor (A) drives a change detector (B) that generates the ON and OFF events (D). Pixel photoreceptors continuously transduce the photocurrent $I_p$ produced by the photodiode (PD) to a logarithmic voltage $V_p$, which results in over 120 dB dynamic range sensitivity. This logarithmic voltage (called brightness here) is buffered by a unity-gain source follower to the voltage $V_{sf}$, which is stored in a capacitor $C_{DVS}$ inside individual pixels, where it is continuously compared to the new input. If the change $V_d$ in log intensity exceeds a critical event threshold, an ON or OFF event is generated, representing an increase or decrease of brightness. The event thresholds $\theta_{on}$ and $\theta_{off}$ are nominally identical for the entire array. The time interval between individual events is inversely proportional to the derivative of the brightness. When an event is generated, the pixel’s location and the sign of the brightness change are immediately transmitted to an arbiter circuit surrounding the pixel array, then off-chip as a pixel address, and a timestamp is assigned to individual events. The arbiter circuit then resets the pixel’s change detector so that a new event can be generated by the pixel. Events can be read out from PDAVIS at up to rates of about 10 MHz. The quiescent (noise) event rate is a few kHz.

Non-idealities of the DVS part of the pixel include 1) finite response time $\tau$ caused by the intensity-dependent RC time constant of the photoreceptor voltage $V_p$ as indicated in the photoreceptor circuit (A), 2) pixel-to-pixel mismatch $\sigma_\theta$ of the brightness change thresholds $\theta_{on}$ and $\theta_{off}$ (D), and 3) noise in the output. These non-idealities lead to background activity and Fixed Pattern Noise (FPN) in the DVS responses and finite DVS motion blur but in typical operating conditions the temporal jitter of event timing is less than 1 ms.

For the frames, the intensity samples are captured by the APS readout circuit (C). The absolute intensity is measured by the photocurrent passing non-destructively through the photoreceptor circuit, where it is integrated onto a capacitor $C_{APS}$, whose voltage $V_{inten}$ is read out via a source follower transistor as $V_{APS}$ similar to conventional CMOS image sensors. At the start of each frame, the global signal RST pulls all pixel $V_{inten}$ high. The reset level of each pixel is read out from $V_{APS}$ through column-parallel Analog to Digital Converters (ADC) (not shown). At the end of integration, TX freezes the sampled $V_{inten}$ signal on $C_{APS}$ and the signal values are read out. Each final intensity sample is the difference between the reset level and signal level. The on-chip column-parallel 10-bit ADCs convert the samples of reset and signal and subtraction is computed in software on the host computer. The
frame-based output can generate videos with a desired exposure time – where all pixels have the same integration (or exposure) time – down to about 10 us and up to the frame interval. Readout speed limits the maximum frame rate to about 50 Hz.

Events and frames are transmitted from the DAVIS chip to a host computer over Universal Serial Bus (USB) via a programmable logic chip. Each frame pixel sample is 10 bits occupying a (non-optimized) 2 bytes. Each event is transmitted using a 16-bit microsecond timestamp and from 2 to 4 bytes address depending on data rate (the DAVIS uses Boahen’s word-serial Address Event Protocol (AER) interface); at high data rate, most events use only 2 bytes for their column address, since events from the same row within a short time interval share the same timestamp.
Supplementary Material 1.2  PDAVIS Characterization Setup

Fig. S2-a depicts the experimental setup used to evaluate the optoelectronic properties for both PDAVIS and Sony polarization cameras when rotating a linear polarization filter at different speeds. A narrow band LED light source (LZ4-00G108, Osram) centered at 520 nm is coupled to a 6” integrating sphere (819D-SF-5.3, Newport). The light exiting the integrating sphere is uniform and depolarized due to the multiple scattering events inside the integrating sphere. A custom-built rotational stage is placed in front of the output port of the integrating sphere. The rotational stage is controlled via a 10:1 stepper gear and a DC motor with a feedback controller. The rotational speed of the stage is controlled from a computer and can rotate up to 3,000 RPM. Due to the feedback controller, the rotational speed is within 10 RPM of the desired value.

![Photo of the characterization bench, built around the integrating sphere to generate an unpolarized light, filtered through either a linear polarizer or a combination of linear polarizer and a QWP to generate different AoP and DoLP profiles while an optical power meter measures the irradiance level. Data is collected with either Sony or PDAVIS sensor.](image1)

**Figure S2:**  a Photo of the characterization bench, built around the integrating sphere to generate an unpolarized light, filtered through either a linear polarizer or a combination of linear polarizer and a QWP to generate different AoP and DoLP profiles while an optical power meter measures the irradiance level. Data is collected with either Sony or PDAVIS sensor. b Experimental setup used for collecting data under high dynamic range and rotating ensemble of six linear polarization filters offset by 30°.

For the first set of experiments, a linear polarization filter (20LP-VIS-B, Newport) is placed in the rotational stage opening. The light emerging from the rotating filter is imaged with either PDAVIS or
Sony’s polarization camera. When a linear polarization filter is rotated in front of the camera, the angle of polarization is varied between 0 and 180 degrees. One full rotation of the linear polarization filter will generate two full cycles of the AoP. The rotational speed of the filter was varied between 60 RPM and 1,000 RPM.

For the second set of experiments, a zero-order QWP filter (20RP34-532, Newport) is placed after the rotational stage housing the linear polarization filter and before the imaging sensor. The orientation of the QWP is fixed while the linear polarization filter is rotated at constant speed. When the linear polarization filter is rotated in front of the camera, both the angle and degree of linear polarization are varied. One full rotation of the linear polarization filter will generate four full cycles of the AoP and DoLP.

Fig. S2-b depicts the experimental setup used to evaluate the high dynamic range and motion blur for both PDAVIS and Sony polarization cameras when rotating an ensemble of six linear polarization filters offset by 30° at different speeds. A narrow band LED light source (LZ4-00G108, Osram) centered at 520 nm is coupled to a 6" integrating sphere (819D-SF-5.3, Newport). The output light from the integrating sphere is incident on the ensemble of linear polarization filters. A high intensity LED is placed behind the filter wheel to provide additional light intensity. The filter wheel is mounted on a motor such that the filters are rotated at different speeds. Images are collected with both Sony and PDAVIS sensors.
Supplementary Material 1.3  Fabrication of PDAVIS

The pixelated PFAs were fabricated on a quartz substrate by Moxtek Inc. The PFA contains four sets of pixels with linear polarization filters offset by 45 degrees. The pixel pitch of the filter array is 18.5 microns and matches the pitch of the pixels in the DAVIS vision sensor. Pixels are isolated by a 2 um-wide metal shield.

The steps (illustrated in Fig. S3) to integrate the PFA with the packaged DAVIS chip are based on a method initially presented by Blair et al. and expanded upon below:

1. The quartz glass with the PFA is glued to a secondary cover glass using a UV activated and optically transparent epoxy (OP-29, Dymax). The cover glass has the same dimensions as the ceramic package of the DAVIS (Fig. S3a).

2. The cover glass is mounted on a 3” by 3” glass plate using thermally activated bonding wax (part number) (Fig. S3b).

3. The glass plate is fixated on a custom-built flat stage and held via vacuum on the stage. The entire stage is fixed using 1” posts on a vibration damped optical table (Fig. S3c).

4. The DAVIS vision sensor is mounted on a 6-Degree of Freedom (DOF) alignment stage and placed under the cover glass stage (H-811 Hexapod, PI-USA Instruments). The alignment stage is initialized to the lowest position with about 2 cm space between the filter array and the sensor plane (Fig. S3d).

5. An integrating sphere (819D-SF-4, Newport) coupled with a high power red led (M660D2, Thorlabs) is placed 2 feet away from the DAVIS sensor. An adjustable iris (SM2D25, Thorlabs) followed by a linear polarization filter (WP25L-VIS, Thorlabs) mounted on a computer-controlled rotational stage (HDR50, Thorlabs) is placed at the output of the integrating sphere. The center of the output port of the integrating sphere is aligned with the center of the vision sensor. Due to the large distance between the integrating sphere and the vision sensor and the small aperture of the iris, the incident light is collimated and linearly polarized (Fig. S3e).

6. Live images are streamed from the DAVIS sensor and custom software is used to provide statistics about the vision sensor, such as the mean and standard deviation of individual pixels in the image array as well as extinction ratios between orthogonal pixels.

7. As the vision sensor is brought closer to the filter array, first the pitch and yaw are adjusted, followed by x- and y- adjustments. For each positional adjustment, the linear polarization filter in front of the vision sensor is rotated, which enables evaluation of the extinction ratios (Fig. S3f).

8. The vision sensor is considered in contact with the pixel array when the extinction ratios remain constant. At this point, the aperture is increased to generate less collimated light. If the extinction ratios remain the same, then the filter is in contact with the sensor.

9. The DAVIS sensor is then lowered away from the filter array. A UV activated epoxy is added to the ceramic package of the DAVIS sensor and the sensor is brought slowly into contact with the filter array. Because the camera was only translated in the z direction during this step, it remains in good alignment with the filter array. Small positional adjustments can be made if necessary. Since the light source used for imaging does not have any UV component, the epoxy does not cure during the alignment process.

10. A UV light source is used to activate the epoxy and permanently attach the filters to the ceramic package. The UV light will cure 99% of the epoxy within the first 15 to 30 seconds. However, 100% of the epoxy is cured after 24 hours of UV exposure. The filters and vision sensors remain in the alignment stage for 24 hours under UV light to completely cure the epoxy.

11. Next, the vacuum is turned off so that the glass plate can be removed from the alignment stage without damaging the vision sensor and glued filters. The camera is lowered and removed from the alignment instrument (Fig. S3g).

12. The glass plate is removed by applying heat from a hot plate at 80 C. Any residual bonding wax on top of the vision sensor is cleaned with acetone-soaked cotton swabs (Fig. S3h).

The completed PDAVIS is shown in Fig. S3. The pixelated polarization filters are aligned and in contact with the DAVIS pixel array. The filters are attached to a secondary cover glass slide and glued to the ceramic package of the DAVIS chip.

Fig. S3 shows an SEM image of the four different orientations of the nanowires within individual pixelated polarization filters.
Figure S3: Fabrication steps of the PDAVIS PFA.  

- **a** Quartz glass with PFA is glued to a cover glass.  
- **b** Cover glass is mounted on a glass plate.  
- **c** Glass plate is vacuum-fixed to flat stage.  
- **d and e** The polarization filter stack is positioned during live operation of the PDAVIS to the die.  
- **f** Polarization filter stack is aligned and attached to the vision sensor.  
- **g** Complete image sensor removed from alignment stage.  
- **h** Glass plate is removed from the polarization sensor.  
- **i** Photo of the assembled PDAVIS. The PFA is attached to the bottom of the coverglass.  
- **j** SEM image of PFA.
Supplementary Material 1.4 Extinction ratio measurements

The following setup is constructed to measure the Extinction Ratio (ER) of PDAVIS as a function of wavelength. We start by using a 400 W halogen light bulb (7787XHP, Philips) housed in a custom box and powered by a high power voltage supply (N5770A, Agilent). The light from the halogen bulb is directed into a monochromator (Acton SP2150, Princeton Instruments), where the desired wavelength is selected using a grating and a computer-controlled slit at the output port. Since the output light beam is typically partially polarized, an integrating sphere (819D-SF-4, Newport) is placed at the output port of the monochromator to depolarize the monochromatic light beam. A pinhole (SM2D25, Thorlabs) followed by an aspherical lens (ACL5040U, Thorlabs) are used to collimate the light beam emerging from the integrating sphere. Lastly, a linear polarization filter (WP25L-VIS, Thorlabs) mounted on a computer-controlled rotational stage (HDR50, Thorlabs) is used to produce collimated and linearly polarised monochromatic light which is imaged by either the PDAVIS sensor or a spectrometer. The spectrometer is used to measure the exact wavelength of the incident light on the vision sensor. An optical power meter is placed at the same location where the image sensor is located and used to measure the photon flux of the incident light at the desired wavelength.

With the setup described above, we first recorded 100 frames with all light blocked from the sensor. These 100 frames, subsequently called dark frames, are temporally averaged to find the digital number offset for each pixel caused by imperfections of the pixel’s circuitry. Next, the monochromator is turned on and set to output monochromatic light at a particular wavelength. The linear polarization filter is rotated 180° in increments of 5°. A total of 100 frames are recorded for each angle and are spatiotemporally averaged over a 42x28 macropixel Region of Interest (ROI). The 180° sweep over a single wavelength gives us one period of Malus’s Law (Supplementary Material 2.1, Eq. (S8)). A non-linear regression then fits the cosine squared signal reconstructed from the linear polarizer sweep. After subtracting the dark frame to remove noise offsets, the ER is computed by taking the ratio of the largest and smallest digital number from the cosine squared function. This process is repeated over the range of wavelengths from 500nm to 700nm in steps of 20nm to give us the extinction ratio for each filter in the macropixel. The results are shown in Figure S4.

![Figure S4: Measured extinction ratios vs. wavelength for the PDAVIS sensor.](image-url)
Supplementary Material 1.5 Dynamic range for polarization sensitivity

To measure the Dynamic Range (DR) over which the PDAVIS or Sony sensors are sensitive to linearly polarized light, we constructed the following optical setup. A custom-built high power, water-cooled white LED light source (CXB3590, Digikey) is coupled to a 4” integrating sphere (819D-SF-4, Newport). The LED power is adjusted by a computer-controlled power supply (N5770A, Agilent). The light exiting the integrating sphere is uniform and depolarized due to the multiple scattering events inside the integrating sphere. A linear polarization filter (WP25L-VIS, Thorlabs) mounted on a computer-controlled rotational stage (HDR50, Thorlabs) is placed at the output of the integrating sphere. The linear polarization filter is rotated at 60 RPM. Hence, time-varying linearly polarized light at different intensity levels is used to illuminate either the PDAVIS or Sony polarization camera.

The Sony camera exposure time is set to 20 ms for this set of optical experiments. This mimics a situation where in order for the dark parts of the imaged scene to have a nonzero digital value, the minimum exposure time should be at least 20 ns. The PDAVIS pixels has a local gain/exposure control by virtue of the logarithmic photoreceptors, and thus there is no need to set any exposure time because the frames are not used for the Deep Neural Network (DNN) reconstruction method. For each illumination levels, both Sony and PDAVIS capture polarization information from a ROI of 20x20 macropixel corresponding to the rotating linear polarization filter. For the Sony camera, AoP is computed from the raw intensity information from the four super pixels and spatially averaged across the ROI. For the PDAVIS, we first reconstruct the intensity for the four individual channels of polarized pixels using the DNN method (which uses only the brightness change events) (see Supplementary Material 2.4), and then computed the spatially averaged AoP within the ROI. Since the linear polarization filter was rotating at a steady speed, the AoP is a repeated sawtooth linear response, sweeping between 0° and 180°. However, once the illumination level exceeds the DR of the camera, the saturated pixels will result in incorrect AoP computation and thus the range of the reconstructed AoP is smaller than the expected 180°.

The Fig. S5 results show the range of AoP reconstruction angles for the sawtooth variation, over illumination level ranging from 40 nW/cm² to 42 mW/cm². It demonstrates that the Sony camera can reconstruct the AoP between 40 nW/cm² and 300 µW/cm² optical flux, corresponding to a dynamic range of 77.5 dB (7300X). Beyond 300 µW/cm² optical flux, all Sony pixels are saturated and the polarization sensitivity vanishes. By contrast, the PDAVIS is able to reconstruct nearly the full 180° sawtooth over 120 dB illumination levels, from 40 nW/cm² to 42 mW/cm² optical power.

**Figure S5:** Measured dynamic range for polarization sensitivity for PDAVIS and Sony’s polarization sensors. The AoP axis is the amplitude of the reconstructed sawtooth as the linear polarization filter is rotated 180 degrees.
Supplementary Material 1.6  PDAVIS and Sony camera specifications

Table 1 compares the design and measured specifications of the PDAVIS with a state-of-the-art Commodity Off-The-Shelf (COTS) frame-based polarization camera (FLIR BFS-U3-51S5), which uses the Sony IMX250 camera chip. Details of our measurements of dynamic range and extinction ratio of PDAVIS precede this section.

The Sony polarization sensor has higher resolution, smaller pixel size, and higher extinction ratio. Our bioinspired sensor is fabricated at several different locations: the event-based sensor is fabricated in a 180nm CIS process provided by TowerJazz Semiconductors; pixelated polarization filters are fabricated in Moxtek cleanroom facilities; the filters and image sensor are integrated at University of Illinois. Due to the complex fabrication steps, the image sensor pixel pitch is larger and the extinction ratios are lower than Sony’s sensor. The PDAVIS offers much higher temporal resolution (≈100 µs versus 12 ms) and its DVS output has superior DR compared to Sony polarization camera (120dB vs 72dB).

Table 1: Specification and comparison

|                      | PDAVIS (this work) | COTS Sony IMX-250 |
|----------------------|--------------------|-------------------|
| CIS Process          | 180nm              | 90/40nm stacked   |
| Pixel size           | 18.5µm             | 3.45µm            |
| Array size           | 346x260            | 2448x2048         |
| Output               | APS+DVS+IMU        | APS               |
| Power consumption (camera) | est. 3 W | 3 W    |
| ER at 500nm          | 40                 | 350               |
| Max APS frame rate   | 53 Hz\(^a\)        | 75 Hz             |
| APS DR               | 52dB\(^c\)         | 72 dB             |
| Max DVS event rate   | 10 MHz             | -                 |
| DVS DR               | 120dB\(^d\)        | -                 |
| DVS Min latency\(^b\) | 3us@1klux\(^d\)   | -                 |
| Min DVS threshold\(^b\) | ±14%            | -                 |
| DVS threshold mismatch\(^c\) | 3.5%\(^d\)       | -                 |

\(^a\) with exposure 80 us.
\(^b\) At room temperature, with mean background leak activity rate of 0.7 Hz with background intensity from APS exposure of 26 DN/ms.
\(^c\) Pixel to pixel 1-σ mismatch of the threshold in temporal contrast.
Supplementary Material 2  Reconstructing polarization information from PDAVIS output

Supplementary Material 2.1 provides the definition of the Stokes parameters, AoP, and DoLP. Supplementary Material 2.2 shows that using only the brightness changes (log intensity changes) signaled by the DVS events from PDAVIS allows us to retrieve (at least) the change in AoP, because it depends on the ratio of differences of polarizer responses. However, for the DoLP the absolute intensity does not cancel, and so it cannot be recovered solely from the brightness change events. The DAVIS APS frames, however, provide periodic absolute intensity samples. These samples have the limited DR and sample rate of frames, but by combining them with the DVS events, we can reconstruct the absolute intensity with larger DR and higher sample rate, and thus polarization at high effective sample rates.

We demonstrate two very different approaches for such absolute intensity reconstruction. The Complementary Filter (CF) (Supplementary Material 2.3) is based on a hand-crafted sensory fusion algorithm CF, which fuses frames and events. The DNN method (Supplementary Material 2.4) is based on DNNs and infers intensity frames from brightness change events, based on its training data. Table 2 compares the methods.

For Figs. 2-3, the plotted AoP and DoLP values are obtained by averaging over a 12 × 12 pixel ROI centered on the rotating polarizer.

Table 2: Comparison of approaches to reconstruct polarization information from the PDAVIS.

|                | DVS | APS | AoP | DoLP | Sampling rate [Hz] | Latency | Op/pixel |
|----------------|-----|-----|-----|------|-------------------|---------|----------|
| Events         | ✓   | -   | ✓   | -    | 10k               | 1 Event | 12       |
| Frames         | -   | ✓   | ✓   | ✓    | 25                | 1 Frame | 8        |
| DNN            | ✓   | -   | ✓   | ✓    | 10k               | 2k Events | 41k    |
| CF             | ✓   | ✓   | ✓   | ✓    | 10k               | 1 Event or 1 Frame | 14     |
Supplementary Material 2.1 Conventional Polarization Imaging

Polarization is commonly described using the Stokes parameters: \((S_0, S_1, S_2)\) defined:\(^4\)

\[
S_0(t) = I_0(t) + I_{90}(t) \tag{S1}
\]

\[
S_1(t) = I_0(t) - I_{90}(t) \tag{S2}
\]

\[
S_2(t) = I_{45}(t) - I_{135}(t) \tag{S3}
\]

where \(I_i\) stands for the light intensity transmitted by the linear polarizer filter with angle \(i\). A fourth Stokes parameter \((S_3)\) describes the circular polarization properties of the light field, which is not detected by the PDAVIS or Sony cameras. The DoLP and the AoP can then be estimated from the Stokes parameters:

\[
\text{DoLP}(t) = \frac{\sqrt{S_1(t)^2 + S_2(t)^2}}{S_0(t)} \tag{S4}
\]

\[
\text{AoP}(t) = \frac{1}{2} \arctan \left( \frac{S_2(t)}{S_1(t)} \right) \tag{S5}
\]

Equivalently, the incident light can be separated into unpolarized and linearly polarized beams, whose fluxes are \(I_{\text{np}}\) and \(I_p\), respectively. We also let the AoP be denoted by \(\theta(t)\) and the total flux received by the photodiode by \(I_t = I_{\text{np}} + I_p\). Thus, the DoLP and the AoP can be defined by:

\[
\text{DoLP}(t) \equiv \frac{I_p(t)}{I_t(t)} \tag{S6}
\]

\[
\text{AoP}(t) \equiv \theta(t) \tag{S7}
\]

Since the intensity is proportional to the square of the electric field strength, the intensity of light passing through each polarizer is given by \(^5\):

\[
I_i(t) = I_t(t) \text{DoLP}(t) \cos[\theta(t) - i] + \frac{I_t(t)}{2}(1 - \text{DoLP}(t)). \tag{S8}
\]

The second term of \(^5\) has the factor \(\frac{1}{2}\) since half of unpolarized light passes through a filter.
Supplementary Material 2.2 Reconstructing AoP from PDAVIS events only

We can reconstruct the change in absolute log intensity $dL$ from an arbitrary starting point by simply integrating the events over time, as first studied experimentally by Brandli, Muller & Delbruck [0]. Pixel nonidealities cause this estimate to drift. The *events* method regards the events as providing high frequency information about the log intensity change. Above a corner frequency $f_{3dB} = 2\pi \omega = 1/(2\pi \tau)$, the events directly update the filtered log intensity estimate, which decays to zero with time constant $\tau$ between events. Since the AoP depends only on ratios of differences of $I_i$ values, the absolute intensity factors out, so we can compute AoP from the reconstructed $I_i$ values.

For every incoming event, the *events* method asynchronously updates the related reconstructed log intensity change $dL = d\log(F)$ as the asynchronous first-order Infinite Impulse Response (IIR) filter (S9):

$$\alpha \leftarrow e^{-\Delta t/\tau}$$
$$dL \leftarrow \alpha dL + p$$

where $\Delta t$ is the time elapsed since last event from the subpixel, $\tau$ is the filter time constant, and $p = [+\theta_{on}, -\theta_{off}]$ is the signed event threshold, which we estimate from the known bias currents using the formulas from Nozaki & Delbruck [0] and then fine tune to match the low frequency frame-based data.

From the $dL$ values, we can compute AoP by exponentiation of $dL$ to obtain the subpixel $I_i$ value, and use the resulting $I_i$ values in (S5). In practice, we use the $dL$ values directly, since generally $|dL| < 1$ and thus $\exp(dL) \approx 1 + dL$. The 1 would be the same for all terms in (S5) and would thus cancel, leaving the $dL$ value.

The $dL$ in (S9) is the high-pass-filtered log intensity, corresponding to the Laplace domain transfer function (S10):

$$H_{dL}(s) \equiv \frac{dL(s)}{\sum p(s)} = \frac{\tau s}{1 + \tau s}$$

where $s$ is the complex frequency, and $\sum p$ is the staircase sum of Dirac delta brightness changes since filter startup.

There are two exactly equivalent descriptions of this filter: $dL$ is a high-pass-filtered log intensity, and it is also a low-pass-filtered derivative of log intensity. Thus, for frequencies well below the $f_{3dB}$ corner frequency $dL \approx \tau dL/dt$, i.e., $dL$ can be considered as a lowpass filtered derivative of $L$, which filters out derivatives above $f_{3dB}$. For frequencies well above $f_{3dB}$, $dL$ is equal to $L$ minus its DC value averaged over the exponential time window $\tau$. If we can assume that this offset is equivalent for each subpixel, then it cancels out in $S_1$ and $S_2$, which are used to compute the AoP.

For the *events* results in Figs. 1 and 2 we used $f_{3dB} = 0.5$ Hz.

**Effect of high pass filter on AoP:** For input frequencies well above $f_{3dB}$, using the $dL$ values in (S5) results in the AoP if we make the reasonable assumption that all $I_x$ have the same mean value. For frequencies below $f_{3dB}$, where $dL \approx \tau dL/dt$, the following computation shows that using $dL$ in the AoP equation (S5) results in the AoP, but with a phase shift of $\pi/4$. First, we use (S8) to compute the derivative of $I_i$, where $i$ is one of the polarizer angles:

$$\frac{\partial I_i(t)}{\partial t} = -2I_i\text{DoLP}(t)\frac{\partial \theta(t)}{\partial t}\sin[\theta(t) - i] \cos[\theta(t) - i]$$

(S11)

Since we only care about measuring a varying AoP, we have assumed that DoLP and $I_i$ are constant.
Now we can plug (S11) into (S5):

\[
\frac{1}{2} \arctan \left( \frac{\partial S_2/\partial t}{\partial S_1/\partial t} \right) =
\]

\[
= \frac{1}{2} \arctan \left( \frac{\partial I_{45}/\partial t - \partial I_{135}/\partial t}{\partial I_0/\partial t - \partial I_{90}/\partial t} \right)
\]

\[
= \frac{1}{2} \arctan \left( \frac{2\sin(\theta - \frac{\pi}{4}) \cos(\theta - \frac{\pi}{4})}{2\sin(\theta) \cos(\theta)} \right)
\]

\[
= \frac{1}{2} \arctan \left( \frac{1 - \tan(2\theta)}{} \right)
\]

\[
= \theta(t) \mod \pi + \frac{\pi}{4}
\]

\[
= \text{AoP}(t) \mod \pi + \frac{\pi}{4}
\]

(S12)

According to (S12), using the temporal derivatives of intensities in (S5) results in the AoP with a constant \(\pi/4\) offset.

In practice, we used signal periodicity to estimate the AoP phase in Fig. 2. Most of our experiments used a stimulus frequency above \(f_{3dB}\), so the output of the AoP from the events method corresponds to the actual AoP without this offset. For example, Fig. 2c shows the reconstructed AoP sawtooth at 30 RPM, corresponding to an AoP frequency of 1 Hz, which is double the \(f_{3dB} = 0.5\) Hz corner frequency.

To lower the effect of mismatch and temporal noise, an event generated by the macropixel \((x, y)\) contributes to update the macropixels within a one pixel radius.

The AoP values are updated as soon as each event is received, creating polarization events as illustrated in Fig. 1c. These asynchronous updates could drive a quick event-driven processing pipeline that exploits the precise timing of events.

Source code for this algorithm is available \[https://github.com/joubertdamien/poladv4\]
Supplementary Material 2.3  Complementary Filter: Reconstructing AoP and DoLP by fusing frames and events

The CF of Scheerlinck\[20\] is complementary because it considers APS frames as providing reliable low frequency intensity (albeit with limited DR), while the DVS events provide reliable high frequency information about brightness (changes). The CF method fuses the high pass filtered log intensity of the events method with low pass filtered frames. At the CF crossover frequency $\omega = 1/\tau = 2\pi f_{3dB}$, the frame and event estimates of log intensity are weighted equally. For lower frequencies, the frame intensities are weighted more, and for higher frequencies, the event-based estimations are weighted more.

The CF also has a computational cost of about 10 operations per DVS event or APS sample, making it attractive for real-time applications.

At each subpixel, the CF updates its log intensity reconstruction $L$ each time the pixel measures either intensity or generates a DVS event. The CF outputs the log intensity $L$ from the most recent log intensity sample or DVS event. For each pixel’s APS intensity sample or DVS event, the asynchronous first-order IIR filter CF update is

$$\alpha \leftarrow e^{-\Delta t/\tau}$$
$$L \leftarrow \alpha L_{\text{DVS}} + p + (1 - \alpha) L_{\text{APS}}$$

where $\Delta t$ is the time since last update, $\tau = 1/(2\pi f_{3dB})$ is the filter time constant, $p = [+\theta_{\text{on}}, -\theta_{\text{off}}]$ is the event’s log intensity change, and $L_{\text{APS}}$ is the log intensity sample. (If the update is for an event, $L_{\text{APS}} = 0$, or if the update is for a frame, $p = 0$.) Since $\Delta t \ll \tau$ (i.e., the update rate is much higher than the time constant), $\alpha \approx 1 - \Delta t/\tau \sim 1$. Removing the APS input from Eq. (S13) gives the events method presented in the previous section (Eq. (S9)).

In the Laplace domain, the CF filter has form (S14):

$$L(s) = \frac{\tau s}{1 + \tau s} \sum p(s) + \frac{1}{1 + \tau s} L_{\text{APS}}(s).$$

Fig. (S6) illustrates the equivalent continuous time $CR$ highpass plus $RC$ lowpass circuit for the CF, along with the weighting of frames and events in the resulting CF transfer function.

For our experiments, we used CF $f_{3dB} = 1.6$ Hz. The AoP and DoLP are periodically computed using the subpixel $L$ values. The user can decide this update rate; by default, the computation occurs at the end of each packet of PDAVIS data.

**Adaptive gain tuning:** The CF method includes a downweighting of the APS samples when $L_{\text{APS}}$ approach their limits, i.e., are under or overexposed [9 Sec. 4.1]. We used this feature to improve the DR of the reconstruction. We set adaptive gain tuning $\lambda = 0.1$ and used the limits $L_1, L_2 = \log(10, 200)$.

**Filter startup:** To avoid the CF filter startup transient, we initialize the filter output state to the first $L_{\text{APS}}$ frame as soon as it is available.

Source code for the original CF implementation, our implementation of CF, and for computing PDAVIS polarization information are open-source:\[9]\[15\]

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\[9\] Original CF implementation of Scheerlinck, Barnes & Mahony [9] | DavisComplementaryFilter | PolarizationComplementaryFilter | Fast C++ implementation
Supplementary Material 2.4  Polarization FireNet: Reconstructing AoP and DoLP from events

The DNN method applied to the PDAVIS data is based on deep learning and infers the intensity sensed by each subpixel using only the brightness change events. It is based on the work of [0], which showed that it is possible to train a deep recurrent neural network to reconstruct video purely from DVS brightness change events, as long as there is motion in the scene. The reconstructed offset level is chosen by the DNN based on the statistics of its training data samples since the DVS output transmits no offset information, but the reconstruction is locally more accurate in comparison to the CF method.

We started with a pretrained FireNet neural network. For the polarization reconstruction, the events are first separated into 4 channels, each corresponding to one pixel of 2-by-2 macropixels. Each channel thus represents one out of four different polarization angles (see Sec. Supplementary Material 1 and Fig. 1). The events are then accumulated into 3D tensors with the same predetermined exposure time window for each channel, which is different from the original FireNet which used constant event-count exposures. This binning requires that the necessary sample rate must be known apriori to obtain a precise reconstruction of the polarization information. To synchronize the four channels, we used a fixed time window in opposition to a fixed event count, because each channel codes for different and sometimes even orthogonal angles of polarization, hence emitting a different number of events. For example, in the DR measurement, the time window is set to 10 ms.

Once we receive the stack of frames from the FireNet, calibration is applied. For the data collected using only a linear polarizer (Fig. 2), we subtract an offset calculated by the minimum value of each of the 4 channels before calculating AoP. For the DoLP calculation, a gain table of the digital numbers paired with its respective multipliers is made for each RPM from one AoP cycle. This table gives us the non linear mapping from logarithmic to linear response for each of the four channels that is used on a second data set to calculate the corrected DoLP. As for the DoLP calculation of the data collected from the linear polarizer and quarter wave plate (Fig. 3), the 4 channels only have an offset and normalization of the max data point applied before DoLP calculation. Then, the FireNet outputs intensity frames from the event tensors, which we use to compute the angle and degree of polarization using Eqs. (S5) and (S4).

Our source code for FireNet reconstruction is available on GitHub.

\[https://github.com/tylerchen007/firenet-pdavis\]
Supplementary Material 3  Bovine tendon preparation and experimental setup

Bovine flexor tendon was sliced using a vibratome to produce 300-micron thick slices. A single sliced tendon is mounted on a 6-DOF computer-controlled actuator and sensor stage. The end pieces of the tendon are clamped via sandpaper to the sensor stage. An LED light source combined with a linear polarization filter (Gray Polarizing Film 38-491, Edmund Optics) and an achromatic QWP (AWQP3, Bolder Vision Optik, Boulder, Colorado) were placed under the bovine flexor tendon. This optical setup generates circularly polarized light which is used to illuminate the tendon. The light that is transmitted through the tissue is imaged with either the PDAVIS or Sony polarization sensor. Both sensors were equipped with x10 optical lens with a numerical aperture of 0.25 (f/2) and placed directly above the tissue.

The tendon is cyclically loaded between 2% and 3% strain at rates of 1, 5, and 10 Hz for 30 seconds. During the cyclical loading of the tissue, the birefringent properties of the individual collagen fibers are modulated as a function of the applied strain. As circularly polarized light is transmitted through the tissue under cyclical load, the light passing through the collagen fibers will both scatter (i.e., depolarized light) and become elliptically polarized. The ellipticity of the polarized light is directly proportional to the strain applied to the collagen fibers. Hence, the degree of linear polarization provides a measurement of the ellipticity of the circularly polarized light and an indirect measure of the applied strain on the tendon.
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