Magnetic field control of the Franck-Condon coupling of few-electron quantum states

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Abstract:
The longitudinal vibration of a suspended carbon nanotube has been observed many times in low temperature transport spectra via distinct harmonic Franck-Condon sidebands. 1-5 Typically, strong Franck-Condon coupling has been attributed to disorder-induced or deliberately targetted charge localization. Here, we present the observation of a strong, tunable coupling in an ultra-clean carbon nanotube with \( N = 1 \) or \( N = 2 \) electrons in the conduction band.

The clean transport spectrum allows a tentative identification of the electronic base quantum states according to their valley quantum number. Interestingly, the Franck-Condon coupling strength \( g \), as extracted from our data, both depends on the magnetic field and on the precise electronic quantum states participating in transport. While spin-dependent Franck-Condon phenomena have already been observed, 6 our results clearly point towards a valley-dependent origin.

As possible cause of this phenomenon, re-shaping of the electronic wavefunction envelope by the magnetic field 7-9 is discussed. A simple calculation demonstrates that variations of \( g \) as observed in the experiment can be reproduced by the theory, paving the way towards more realistic and detailed quantum-mechanical modelling.

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