Noise Analysis of Open-Loop and Closed-Loop SAW Magnetic Field Sensor Systems

Phillip Durdaut, Student Member, IEEE, Anne Kittmann, Enrico Rubiola, Member, IEEE, Jean-Michel Friedt, Eckhard Quandt, Reinhard Knöchel, Life Fellow, IEEE, and Michael Höft, Senior Member, IEEE

Abstract—Transmission surface acoustic wave (SAW) sensors are widely used in various fields of application. In order to maximize the limit of detection (LOD) of such sensor systems, it is of high importance to understand and to be able to quantify the relevant noise sources. In this paper, low noise readout systems for the application with a SAW delay line magnetic field sensor in an open-loop and closed-loop configuration are presented and analyzed with regard to their phase noise contribution. By applying oscillator phase noise theory to closed-loop sensor systems, it is shown that the phase noise of the SAW delay line oscillator can be predicted accurately. This allows the derivation of expressions for the limits of detection for both readout structures. Based on these equations, the equivalence between the LOD of open-loop and closed-loop SAW delay line readout can be shown analytically, assuming that the sensor contributes the dominant phase noise. This equality is verified by measurements. These results are applicable to all kinds of phase sensitive delay line sensors.

Index Terms—Delay line sensors, frequency detection, magnetic field detection, open-loop vs. closed-loop, phase detection, readout systems, sensors, surface acoustic wave

I. INTRODUCTION

Surface acoustic wave (SAW) devices started to become attractive with the invention of the interdigital transducer (IDT) in 1965 [1] which allows to excite SAWs on piezoelectric substrates in an efficient way. Advantages properties like small size, low cost, and high reproducibility [2] make SAW technology very attractive for sensor applications [3], [4]. Among many others, SAW sensors for measuring temperature [5], [6], pressure [7], [8], magnetic fields [9]–[23], humidity [24], and vibration [25] or for the detection of gases [26] and biorelevant molecules [27], [28], respectively, have been reported.

A SAW is excited by applying an electrical field on an IDT that is patterned on a piezoelectric material. The resulting mechanical wave propagates perpendicular to the direction of the IDT in both directions on the surface of the piezoelectric substrate with typical wave velocities between 3000 m/s and 5000 m/s [4], [29]. For sensing applications the substrate’s surface is frequently coated with an additional layer which reacts to changes of the physical quantity to be measured, and in turn alters the SAW in its amplitude and in its velocity.

Throughout this paper, we solely focus on a two-port delay line sensor that comprises two IDT electrodes placed in some distance to each other. A sensing layer between the IDTs attenuates and affects the velocity of the propagating wave in dependence of the physical quantity to be measured. Because a surface acoustic wave is traveling about five orders of magnitude slower compared to the electromagnetic propagation the delay line results in typical group delays $\tau_g$ from several hundred nanoseconds to several microseconds, depending on the SAW device’s size.

There are two different schemes for the readout of SAW delay line sensors. A straightforward approach is to compare the phase of the sensor’s output signal with a reference phase [29] in an open-loop system, thus creating a delay line phase discriminator [30], [31]. Alternatively, readout of such sensors can be achieved with a closed-loop approach by including the sensor into the feedback loop of an oscillator, thus changing oscillation frequency with the sensing function [32]–[34]. Both approaches might suffer from noise which is introduced into the sensor system by the required electrical components. However, even if all the electronic components are designed very carefully such that their noise contributions can be neglected, one crucial question remains: Is one of these approaches superior to the other regarding the overall achievable limit of detection (LOD)? Recently, we addressed this question in a theoretic study [35]. In this paper, a SAW magnetic field sensor is operated in open-loop configuration and in a closed-loop system. Based on phase noise measurements of the individual electronic components of both systems, the earlier presented expressions for the phase noise and the LOD are verified.

This paper is organized as follows: Sec. II briefly introduces the SAW magnetic field sensor utilized in this investigation. Based on the sensor-specific requirements open-loop and closed-loop readout systems are presented in Sec. III. A comparison regarding the readout system’s overall phase noise is presented in Sec. IV based on the individual phase noise contributions of both the electrical components and the sensor-intrinsic noise. This article ends with a summary in Sec. V.

II. SAW SENSOR

The utilized SAW delay line sensor has been produced in the Kiel Nanolaboratory and is based on a 500 μm thick ST-cut quartz substrate. A delay line is formed using two split-finger
IDT electrodes with 25 finger pairs, a periodicity of 28 \( \mu m \) and a finger width of 3.5 \( \mu m \) with an IDT center-to-center length of \( L = 4.64 \) mm. A SiO2 layer with a thickness of 4.5 \( \mu m \) deposited on top of the IDTs and the delay line acts as a guiding layer for the surface acoustic Love wave. A magnetostrictive material (Fe80Co20)78Si12B10 with a thickness of 200 nm and a length of 3.8 mm is deposited on top of the guiding layer and between the IDTs. Further details about the fabrication can be found in [21].

The sensor principle [21] is based on the magnetoelastic effect which changes the shear modulus of the magnetostrictive material as a function of the material’s magnetization, i.e. by a surrounding magnetic flux density \( B \). Due to the relation between the elastic properties and the wave’s propagation velocity [10], the phase angle \( \varphi \) of the sensor signal changes with the magnetic flux density \( B \).

For this type of sensor, not only the expected dependence of the magnetic sensitivity \( S_{mag} \) on a DC magnetic bias flux density \( B_{bias} \) exists. Also strong interdependencies between the magnetic insertion loss \( IL_{mag} \), the sensor’s intrinsic phase noise and both the SAW input power \( P_{SAW} \) and \( B_{bias} \) are observed. Further details about the magnetic properties as well as the noise behavior of this kind of sensor will be published in the near future. Generally, an additional DC bias flux density \( B_{bias} \) can be applied to optimize the phase noise behavior and thus, the limit of detection (LOD). However, this requires the sensor to be surrounded by an additional coil fed by a current from an ultra-low noise current source which is also capable of providing relatively high currents in order to perform a certain magnetic saturation prior to the measurements. Yet, the sensor used in this investigation is quite suited to operate without any DC bias flux density. For simplification, and because the focus in this article is on the readout systems, the magnetic operating point is set to \( B_{bias} = 0 \). Tab. I summarizes the most important electrical and magnetic properties of the SAW magnetic field sensor in its operating point.

### III. READOUT SYSTEMS

The developed open- and closed-loop readout systems are depicted in Fig. 1 together with the according power levels. Both systems are mostly based on RF components by Mini-Circuits with all their identifiers given in the system diagrams. In order to allow a comparison between both methods care has been taken to feed the SAW sensor in each case with the same input power of \( P_{SAW} = 0 \) dBm because the SAW sensor’s intrinsic phase noise is a function of \( P_{SAW} \).

#### A. Open-Loop System

The open-loop readout system (Fig. 1a) is based on a heterodyne structure in which the output signal of a phase stable numerically controlled oscillator (NCO) with a frequency of 50 kHz is upconverted to the SAW device’s passband at \( f_0 = 144.8 \) MHz by means of a single sideband (SSB) upconverter and a local oscillator (LO). The SSB upconverter suppresses the undesired lower sideband which would also fall into the passband of the SAW device and which represents the image frequency with regard to the subsequent downconverter.

| TABLE I: Summary of the electrical and magnetic properties of the utilized magnetic field SAW sensor in its operating point. |
|---------------------------------------------------------------|
| Length of the delay line | Acoustic wavelength |
|--------------------------|----------------------|
| \( L = 4.64 \) mm | \( \lambda = 28 \) \( \mu m \) |
| Center frequency | \( f_0 = 144.8 \) MHz |
| \(-3\) dB bandwidth | \( \Delta f = 4.6 \) MHz |
| Return loss | RL > 20 dB |
| Insertion loss of the delay line | \( I_{L_{elec}} = 20 \) dB |
| Magnetic loss | \( I_{L_{mag}} = 8 \) dB |
| Overall insertion loss | \( I_{L} = I_{L_{elec}} + I_{L_{mag}} = 28 \) dB |
| Phase velocity | \( v_\varphi = f_0 \lambda = 4054 \) m/s |
| Phase delay | \( \tau_\varphi = L/v_\varphi = 1145 \) ns |
| Phase slope of the delay line | \( \partial \varphi/\partial f = -8.73 \) rad/MHz |
| Group delay | \( \tau_g = \partial \varphi/\partial f = 2 \pi = 1389 \) ns |
| Group velocity | \( v_\varphi = L/\tau_g = 3341 \) m/s |
| Electrical sensitivity | \( S_{elec} = 2 \pi \tau_g = 8.73 \) rad/MHz |
| Magnetic sensitivity | \( S_{mag} = \varphi/\partial B = 16.5 \) rad/mT |
| SAW input power | \( P_{SAW} = 0 \) dBm |
| Magnetic operating point | \( B_{bias} = 0 \) |
| Sensor’s phase noise \( S_\varphi(f) \) | See Fig. 3 |

Sufficient sideband suppression (typically about \(-60 \) dB) is achieved by adjusting both amplitude and phase of the SSB converter drive signals numerically. The SSB upconverter consists of a 2-way-90\(^\circ\) power splitter ZMSCQ-2-180+ at the input and a 2-way-0\(^\circ\) combiner ZMSC-2-1W+ at the output. In-between, two level-17 mixers ZAD-1H+ perform the frequency conversion. The sensor’s output signal is amplified and downconverted to the original frequency of 50 kHz utilizing a double sideband (DSB) mixer using the same LO. Thus, the phase noise of the high-frequency LO is largely suppressed. In fact, the degree of phase noise suppression depends on the group delay \( \tau_g \) of the SAW sensor and on the offset frequency [36]. Assuming a sinusoidal magnetic flux density to be measured \( B_s(t) = B_s \cos(2\pi f_s t) \) the sensor’s output signal

\[
s_{PM}(t) \propto \cos(2\pi f_0 t + S_{PM} B_s \cos(2\pi f_s t) + \psi_{OL}(t))
\]  \( (1) \)

is phase modulated (PM) by \( B_s(t) \) with a sensitivity of \( S_{PM} = S_{mag} = 16.5 \) rad/mT (\( \approx 945 \) °/mT). From basic modulation theory, it is well-known that the modulation index \( \eta_{PM} = S_{PM} B_s \) is linked to the carrier-to-sideband ratios of phase-modulated signals by Bessel functions of the first kind \( J_n(\eta_{PM}) \), where \( n \) is the number of the sideband (SB) [37, p. 141 ff.]. Based on this relationship, prior to the noise measurements, the modulation purity and thus, the sensitivity \( S_{PM} \) is verified by a series of measurements for various amplitudes \( B_s \) of the signal to be measured with the results shown in Fig. 2a. In Eq. (1) \( \psi_{OL}(t) \) describes the overall phase noise of the open-loop system, i.e. the phase noise of the SAW sensor and the phase noise of the electronic readout system. Both, the contribution of the sensor as well as the individual contributions of the various electrical components will be analyzed in Sec. IV.
(a) Open-loop readout system with inherent phase noise suppression of the high-frequency local oscillator. A low phase noise signal of a numerically controlled oscillator with a frequency of 50 kHz is transposed to the SAW sensor’s operating frequency \( f_0 = 144.8 \) MHz and received using a floating local oscillator, which largely suppresses its phase noise. Phase detection is performed in the digital domain after analog-to-digital conversion.

(b) Closed-loop readout system with the SAW sensor included in the feedback loop of an amplifier leading to an oscillation with a frequency of approx. \( f_0 = 144.8 \) MHz. A limiter is used to stabilize the SAW sensor’s input power to 0 dBm. Frequency detection is performed in the digital domain after downconverting the oscillation signal to an intermediate frequency of 50 kHz and subsequent analog-to-digital conversion.

Fig. 1: Developed open- and closed-loop readout systems for the determination of the applied magnetic field. In the open-loop systems a magnetic flux density to be measured leads to a phase modulation of the SAW sensor’s output signal whereas the same leads to a frequency modulation in the closed-loop oscillator.

B. Closed-Loop System

The structure of the closed-loop readout system is shown in Fig. 1b. The SAW sensor is included in the feedback branch of an amplifier which compensates for the sensor’s insertion loss, and thus leads to an oscillation at approx. \( f_0 = 144.8 \) MHz. An additional limiter is used to stabilize the SAW sensor’s input power to 0 dBm. Because of the sensor’s linear phase response over a wide frequency range with a slope of \( \partial \phi / \partial f = -8.73 \text{rad/MHz} \), oscillations with a frequency spacing of \( \delta f_0 = 1/\tau_0 \approx 720 \text{kHz} < \Delta f \) are generally possible. Therefore, an additional phase shifter is not needed. Utilizing a \(-10 \) dB directional coupler the oscillator signal is coupled into a mixer for downconversion to an intermediate frequency of 50 kHz in order to perform the subsequent analog-to-digital conversion and the demodulation. Assuming again a sinusoidal magnetic flux density to be measured \( B_x(t) = B_x \cos(2\pi f_x t) \) the oscillator signal

\[
s_{FM}(t) \propto \cos \left( 2\pi f_0 t + \frac{S_{FM} B_x}{f_x} \sin(2\pi f_x t) + \psi_{CL}(t) \right)
\]

(2)

is frequency modulated (FM) by \( B_x(t) \) with a sensitivity \( S_{FM} \) described by the open-loop system, the FM purity and the sensitivity \( S_{FM} \) is verified by measurement of the carrier-to-sideband ratios and subsequent comparison with the theoretical expectations according to the Bessel functions of the first kind \( J_n(\eta_{FM}) \). The results are shown in Fig. 2b in which the variance of the measured amplitudes is distinctly higher as for the PM case because of the high phase noise in the closed-loop-system. In Eq. (2) \( \psi_{CL}(t) \) describes the overall oscillator phase noise of the closed-loop system, i.e. the phase noise due to the SAW sensor and due to the electronic readout system, both further discussed in Sec. IV.

IV. Noise Analysis

Random fluctuations of an arbitrary phase \( \phi(t) \) are best described by the one-sided power spectral density of the random phase fluctuations \( S_{\phi}(f) \) in units of \( \text{rad}^2/\text{Hz} \). For historical reasons, phase noise analyzers give the results in terms of a phase noise density spectrum \( \mathcal{L}(f) \) which is defined as \( \mathcal{L}(f) = 1/2 S_{\phi}(f) \) and usually given in units of dBc/Hz [38], [39]. In order to simplify mathematical expressions and to stay with SI units, \( S_{\phi}(f) \) is used throughout this article. The logarithmic representation \( 10 \log_{10}(S_{\phi}(f)) \) is then given in units of dB rad\(^2\)/Hz. A useful model for describing the
frequency dependence of a power spectral density of random phase fluctuations is the polynomial law

$$S_p(f) = \sum_{i=-n}^{0} b_i f^i$$

(3)

with usually $n \leq 4$. $i = 0$ and $i = -1$ refer to white phase noise and $1/f$ flicker phase noise, respectively, which are the main processes in two-port components [40, p. 23] [41]. As will be shown further below, in closed-loop systems white phase noise results in white frequency noise ($i = -2$) and flicker phase noise results in flicker frequency noise ($i = -3$). Higher order effects like random walk of frequency ($i = -4$) are related to environmental changes like e.g. temperature drifts, humidity, and vibrations [42]. All phase noise measurements were performed utilizing a Rohde & Schwarz FSWP phase noise analyzer.

### A. SAW Sensor

For the measurement of the power spectral density of the random phase fluctuations of the magnetically coated SAW device $S_{pSAW}(f)$, the sensor has been placed inside an ultra high magnetic field shielding mu-metal cylinder ZG1 from Aaronia AG in order to avoid environmental magnetic distortions. For the sensor in its operating point (blue line in Fig. 3) of $B_{\text{min}} = 0$ the measurement reveals a $1/f$ flicker phase noise which can be quantified properly by $b_{-1} = 8 \times 10^{-11} \text{rad}^2$. If the sensor is magnetically saturated utilizing a strong permanent magnet (green line in Fig. 3) the flicker phase noise decreases by more than 20 dB, indicating that the sensor’s resolution is limited by magnetic magnetic noise, e.g. magnetic domain wall motions. The underlying mechanisms and possibilities to reduce the flicker phase noise are currently still under investigation. Although both measurements were conducted for an input power of $P_{\text{SAW}} = 0 \text{dBm}$ the white phase noise level differs because under magnetic saturation the insertion loss decreases. Note that both white phase noise floors are slightly impaired by an utilized preamplifier (ZFL-1000LN+ from Mini-Circuits with a noise figure of $F \approx 3 \text{dB}$) at the RF input of the phase noise analyzer.

### B. Open-Loop System

For the open-loop system, Fig. 4a depicts the measured phase noise contributions of the various electrical components. The high phase noise of the LO with values of $-31 \text{ dB rad}^2/\text{Hz}$ at 1 Hz and $-74 \text{ dB rad}^2/\text{Hz}$ at 10 Hz (not shown for clarity) is largely suppressed in the downconverter stage. The degree of phase noise suppression as a function of the frequency and the sensor’s group delay

$$PNS(f, \tau_g) = 20 \log_{10} (2 \sin (\pi f \tau_g)) \text{dB}$$

(4)

has already been determined and was experimentally verified in previous investigations [35], [36]. Thus, the SAW sensor dominates the overall phase noise for frequencies $< 1 \text{kHz}$. At $f = 1 \text{Hz}$ the mixers and the amplifier contribute a phase noise density of approx. $-120 \text{ dB rad}^2/\text{Hz}$. With values $< -135 \text{ dB rad}^2/\text{Hz}$, the phase noise of the NCOs, i.e. the in-phase and quadrature (IQ) signals are negligible at low frequencies. However, for frequencies $> 1 \text{kHz}$ the sum of the phase noise contributions of the various electrical components become dominant and result in a white phase noise level of $7.5 \times 10^{-14} \text{ rad}^2/\text{Hz}$. 
the SAW sensor, Fig. 4b shows the measured phase noise of the individual components of the open-loop SAW sensor system together with their sum. In addition to the intrinsic noise of the limiter and of the directional coupler, the phase noise of the SAW sensor and the amplifier. The phase noise spectra of the open-loop system (mixers, amplifier, NCOs, and LO with PNS) shown in Fig. 4a. Please note that Eq. (4) and Eq. (5) are simplified expressions for delay line sensors offering bandwidths higher than the frequency to be analyzed, which is true for the sensors under investigation. More accurate expressions for narrow band delay line sensors can be found in [35].

\[
\text{LOD}_{PM}(f) = \frac{S_{\psi\text{OL}}(f)}{S_{PM}},
\]

where \(S_{\psi\text{OL}}(f)\) is the power spectral density of the fluctuating phase \(\psi_{\text{OL}}(t)\) introduced in Eq. (1). This power spectral density is the sum of both, the phase noise of the SAW sensor and the phase noise contributions of all other electrical components of the open-loop system (mixers, amplifier, NCOs, and LO with PNS) shown in Fig. 4a. Please note that Eq. (4) and Eq. (5) are simplified expressions for delay line sensors offering bandwidths higher than the frequency to be analyzed, which is true for the sensors under investigation. More accurate expressions for narrow band delay line sensors can be found in [35].

C. Closed-Loop System

For the noise analysis of the closed-loop system only the contributions of the electrical components inside the oscillator loop are relevant. In fact, these are only the phase noise of the SAW sensor and the amplifier. The phase noise spectra of the limiter and of the directional coupler are actually not measurable with the Rohde & Schwarz FSWP phase noise analyzer in a reasonable time because values as low as approx. \(-180\, \text{dB rad}^2/\text{Hz}\) at 10 Hz can be typically found for such passive devices [43]. In addition to the intrinsic noise of the SAW sensor, Fig. 4b shows the measured phase noise of the amplifier and a rough estimation of the contributions of the passive components utilized inside the oscillator loop. Both the noise contributions of the passive components and the amplifier are negligible for \(f < 8\, \text{kHz}\). Actually, the influence of the amplifier above this frequency could easily be further decreased by utilizing a fixed-gain amplifier instead of a variable-gain amplifier used here. In order to calculate the LOD for the closed-loop sensor system it is necessary to convert the phase noise of the individual components into oscillator phase noise at the output of the oscillator, i.e. at the output of the directional coupler. Following the derivations in [35], random phase fluctuations \(\varphi(t)\) fed into an ideal delay line oscillator result in oscillator phase noise \(\psi(t)\) according to the transfer function

\[
|H(f)|^2 = \frac{|\Psi(f)|^2}{|\Phi(f)|^2} = \frac{1}{1 - e^{-2\pi f \tau_B}} = \frac{1}{2 \left(1 - \cos(2\pi f \tau_B)\right)} = \frac{1}{4 \sin^2(\pi f \tau_B)},
\]

where \(\Phi(f)\) and \(\Psi(f)\) represent the Fourier transforms of the fluctuating phases \(\varphi(t)\) and \(\psi(t)\). A more general representation of this transfer function which also takes into account the frequency-selective characteristic of narrow band delay line sensors is given in [35]. However, the SAW sensor under investigation offers a relatively high \(-3\, \text{dB}\) bandwidth of \(\Delta f = 4.6\, \text{MHz}\), such that the approximation in Eq. (6) is valid for the frequency range of up to 1 MHz analyzed in the following (Fig. 4 and Fig. 5). The power spectral density of the
SAW delay line oscillator’s overall random phase fluctuations is then given by
\[ S_\psi^{CL}(f) = |H(f)|^2 S_\psi^{CL}(f). \] (7)

The sum of the phase noise contributions of the SAW sensor, the amplifier, and the (negligible) passive components \( S_\psi^{CL}(f) = S_\psi^{SAW}(f) + S_\psi^{AMP}(f) \) shown in Fig. 4b are converted into oscillator phase noise \( S_\psi(f) = S_\psi^{SAW}(f) + S_\psi^{AMP}(f) \) using Eq. (7) and are shown in Fig. 4c. As one would expect, the SAW sensor is still contributing the dominant noise for \( f < 8 \text{ kHz} \) whereas the overall noise floor is limited by the amplifier’s noise for \( f > 8 \text{ kHz} \). The sum of the individual contributions (dotted line) perfectly agrees with a direct measurement of the oscillator’s phase noise, and thus confirms the transfer function \( |H(f)|^2 \) from Eq. (6). Even the predicted increase in oscillator phase noise at \( f = 1/\tau_g \approx 720 \text{ kHz} \), due to the pole of the transfer function, perfectly matches the measurement. With the relation between the power spectral density of arbitrary random phase fluctuations \( S_\psi(f) \) and the power spectral density of frequency fluctuations \( S_{\Delta f_0}(f) = f^2 S_\psi(f) \) [42] in units of Hz²/Hz and for a carrier signal of frequency \( f_0 \), the LOD of the closed-loop magnetic field sensor system in units of T/√Hz can be calculated [35] by
\[ \text{LOD}_{FM}(f) = \frac{\sqrt{S_{\Delta f_0}(f)}}{S_{FM}} = \frac{\sqrt{f^2 S_\psi^{CL}(f)}}{S_{FM}} = \frac{f |H(f)| \sqrt{S_\psi^{CL}(f)}}{S_{FM}}. \] (8)

D. Comparison of the Limit of Detection (LOD)

Both expressions for the LOD in the open-loop and for the closed-loop sensor system (Eq. (5) and (8)) directly scale with the amplitude spectral densities of the randomly fluctuating phase of the SAW sensor and the readout electronics. Thus, depending on how carefully the readout systems are designed in terms of phase noise, the LOD can differ. However, as shown for both systems the SAW sensor contributes the dominant phase noise at least for frequencies \( < 1 \text{ kHz} \). Thus, when assuming that the SAW sensor contributes the dominant phase noise in each system, equality between \( \text{LOD}_{FM}(f) \) and \( \text{LOD}_{PM}(f) \) can easily be shown. With Eq. (6) and for frequencies \( f \ll \Delta f \) Eq. (8) can be written as
\[ \text{LOD}_{FM}(f) \approx \frac{f \sqrt{S_\psi^{SAW}(f)}}{2\sin(\pi f \tau_g) S_{FM}}. \] (9)

Replacing both the sine with a small-angle approximation \( \sin(x) \approx x \) which is valid for \( f \tau_g \ll 0.1 \) and replacing \( S_{FM} \) with the previously defined closed-loop sensitivity \( S_{FM} = S_{mag}/S_{elec} = S_{mag}/(2\pi \tau_g) \), Eq. (9) yields
\[ \text{LOD}_{FM}(f) \approx \frac{2\pi f \tau_g}{2\tau_g} \frac{S_\psi^{SAW}(f)}{S_{mag}}. \] (10)

With the definition of the open-loop sensitivity \( S_{PM} = S_{mag} \), Eq. (10) then virtually equals the LOD of the open-loop system
\[ \text{LOD}_{FM}(f) \approx \frac{\sqrt{S_\psi^{SAW}(f)}}{S_{mag}} = \text{LOD}_{PM}(f). \] (11)

For both sensor systems presented in Sec. III the LOD was measured as described in [21] and compared with calculations based on Eq. (5) and (8). The results are shown in Fig. 5 and reveal that the measured LODs not only agree with their according predictions but also that the results are the same for open-loop (PM) and closed-loop (FM) operation for frequencies \( < 1 \text{ kHz} \). A value of approx. 170 pT/√Hz is reached at a frequency of 10 Hz.

E. Time Domain Uncertainty

The output of a sensor system is most often exploited as a stream of data. Designing a system, it is wise to set the averaging time \( \tau \) (please do not mistake \( \tau \) with the phase delay \( \tau_g \) or the group delay \( \tau_g \)) equal to the sampling interval. This is an efficient use of the information because there is no overlap between measurements, and no dead time. A longer \( \tau \) results in higher rejection of white noise, and in turn a lower uncertainty, at the cost of a slower data rate. The question about the optimum measurement time \( \tau_{opt} \), beyond which the uncertainty no longer improves, is best answered describing the fluctuations in terms of the Allan variance (AVAR) [44], [45]. The Allan variance of an arbitrary quantity \( y(t) \), denoted by \( \sigma_y^2(\tau) \), is an extension of the regular variance that makes the measurement time \( \tau \) appear explicitly, and also converges in the presence of flicker noise, random walk and drift. Describing random fluctuations of \( y(t) \) by the power spectral density \( S_y(f) = h_{-1}/f + h_0 \), it holds that \( \sigma_y^2(\tau) = 2\ln(2)h_{-1} + h_0/(2\tau) \). We have shown in [35] that the optimum measurement time is
\[ \tau_{opt} = \frac{1}{4\ln(2)f_c} \approx 0.36 \frac{1}{f_c} \] (12)
where \( f_c = h_{-1}/h_0 \) is the corner frequency where the flicker noise crosses the white noise.
For the open-loop system, we identify the quantity \( y(t) \) with the random phase \( \varphi(t) \), thus \( h_{\varphi} = h_{\varphi}. \) With a flicker phase noise of \( b_{\varphi}\approx 8 \times 10^{-11} \text{rad}^2 \) and white phase noise of \( b_{\varphi0} = 7.5 \times 10^{-14} \text{rad}^2/\text{Hz} \) (Fig. 4a) the crossover frequency yields

\[
f_{CLO}^{OL} = \frac{h_{\varphi}}{b_{\varphi0}} = \frac{b_{\varphi}}{b_{\varphi0}} = 1.07 \text{kHz}. \quad (13)
\]

For the closed-loop system, we identify the quantity \( y(t) \) with the fractional frequency fluctuation \( (\Delta f_{0})/f_{0} \). Thus

\[
h_{\varphi} = b_{\varphi}/f_{0} \text{ and } b_{\varphi0} = b_{\varphi}/f_{0}^{2}. \quad (13)
\]

With a flicker frequency noise \( b_{\varphi} = 1.05 \text{rad}^2/\text{Hz} \) and white noise frequency of \( b_{\varphi0} = 1.3 \times 10^{-3} \text{rad}^2/\text{Hz} \) (Fig. 4c) the crossover frequency yields

\[
f_{CLO}^{CL} = \frac{h_{\varphi}}{b_{\varphi0}} = \frac{b_{\varphi}}{b_{\varphi0}} = 8.08 \text{kHz}. \quad (14)
\]

Thus, for the presented readout systems, the optimum measurement times differ and result in \( \tau_{CLO} \approx 338 \mu s \) and \( \tau_{CL} \approx 45 \mu s. \) The equivalent magnetic uncertainties then yield \( \sigma_{y}^{OL}(\tau_{CLO})/S_{PM} \approx 903 \text{pT} \) for the open-loop system and \( \sigma_{y}^{CL}(\tau_{CL})/S_{FM} \approx 904 \text{pT} \) for the closed-loop system. For ideal sensor systems, in which the sensor contributes the dominant phase noise for all frequencies, \( \tau_{opt} \) would be the same for both readout systems [35].

V. Conclusion

Based on the electrical and magnetic properties of a SAW delay line magnetic field sensor low noise readout systems for the detection of the magnetic signal in an open-loop and closed-loop configuration, respectively, are presented and compared. By analyzing the phase noise contributions of the individual electrical components of each readout system it is revealed that the sensor itself contributes the dominant phase noise for a wide range of frequencies. In particular, it is shown that the phase noise of the SAW delay line oscillator, i.e. the closed-loop system, can be accurately predicted such that according expressions for the calculation of the limits of detection can be derived. Based on these equations equality between the LOD of open-loop and closed-loop SAW delay line readout can be shown even analytically assuming that the sensor contributes the dominant phase noise. This equality is verified by according measurements. These results are applicable to all kinds of phase sensitive delay line sensors. Therefore, the decision-making process for selecting a certain readout structure for a given sensor should mainly be based on the possibility to reduce the electronic phase noise contribution. However, only open-loop systems allow for the characterization of the sensor’s transmission properties as well as to identify the optimum operating point.

Acknowledgment

This work was supported (1) by the German Research Foundation (Deutsche Forschungsgemeinschaft, DFG) through the Collaborative Research Centre CRC 1261 Magnetoelectric Sensors: From Composite Materials to Biomagnetic Diagnostics, (2) by the ANR Programme d'Investissement d'Avenir (PIA) under the Oscillator IMP project and the FIRST-TF network, and (3) by grants from the Région Bourgogne Franche Comté intended to support the PIA. In addition, the authors would like to thank Wolfgang Taute for fruitful discussions and practical help during the development of the readout electronics.

References

[1] R. M. White and F. W. Voltmer, “Direct piezoelectric coupling to surface elastic waves,” Applied Physics Letters, vol. 7, no. 12, pp. 314–316, 1965.
[2] C. Ruppell, R. Dill, A. Fischerauer, G. Fischerauer, W. Gawlik, J. Machui, F. Muller, L. Reindl, W. Ruile, G. Scholl, I. Schropp, and K. C. Wagner, “SAW Devices for Consumer Communication Applications,” IEEE Transactions on Ultrasonics, Ferroelectrics, and Frequency Control, vol. 40, no. 5, pp. 438–452, 1993.
[3] R. M. White, “Surface Acoustic Wave Sensors,” in 1985 IEEE Ultrasonics Symposium, Oct. 1985, pp. 490–494.
[4] B. Liu, X. Chen, H. Cai, M. Mohammad Ali, X. Tian, L. Tao, Y. Yang, and T. Ren, “Surface acoustic wave devices for sensor applications,” Journal of Semiconductors, vol. 37, no. 2, pp. 021 001 1–9, 2006.
[5] J. Neumeister, R. Thum, and E. Luder, “A SAW Delay-line oscillator as a high-resolution temperature sensor,” Sensors and Actuators: A. Physical, vol. 22, no. 1–3, pp. 670–672, 1989.
[6] D. Hauden, G. Jailet, and R. Coquerel, “Temperature Sensor Using SAW Delay Line,” in 1981 IEEE Ultrasonics Symposium, Oct. 1981, pp. 148–151.
[7] H. Scherr, G. Scholl, F. Seifert, and R. Weigel, “Quartz pressure sensor based on SAW reflective delay line,” in 1996 IEEE Ultrasonics Symposium, vol. 1, no. 2, 1996, pp. 347–350.
[8] M. Jungwirth, H. Scherr, and R. Weigel, “Micromechanical precision pressure sensor incorporating SAW delay lines,” Acta Mechanica, vol. 158, no. 3-4, pp. 227–232, 2002.
[9] D. C. Webb, D. W. Forrest, A. K. Ganguly, and C. Vittoria, “Applications of amorphous magnetic-layers in surface-acoustic-wave devices,” IEEE Transactions on Magnetics, vol. 15, no. 6, pp. 1410–1415, 1979.
[10] P. Smole, W. Ruile, C. Korden, A. Ludwig, E. Quandt, S. Krassnitzer, and P. Pongratz, “Magnetically tunable SAW-resonator,” 2003 IEEE International Frequency Control Symposium, no. 2, pp. 4–7, 2003.
[11] M. Kadota, S. Ito, Y. Ito, T. Hada, and K. Okaguchi, “Magnetic sensor based on surface acoustic wave resonators,” Japanese Journal of Applied Physics, vol. 50, no. 7S, 2011.
[12] W. Y. Li, P. Dhatag, and A. Jander, “Surface Acoustic Wave Magnetic Sensor using Galfenol Thin Film,” IEEE Transactions on Magnetics, vol. 48, no. 11, pp. 4100–4102, 2012.
[13] P. Bocchiaro and A. Zamperini, “Surface Acoustic Wave Based Magnetic Sensors,” Modeling and Measurement Methods for Acoustic Waves and for Acoustic Microdevices, pp. 355–380, 2013.
[14] M. Elhosni, O. Elmazria, S. Petit-Watelot, L. Bouvot, M. Henh, A. Talbi, N. Tiercelin, V. Preobrazhensky, P. Pernod, and O. Boumatar, “Theoretical and experimental study of layered SAW magnetic sensor,” in IEEE International Ultrasonics Symposium, IUS, 2014, pp. 874–877.
[15] W. Wang, Y. Jia, X. Liu, and S. He, “Development of a novel SAW Current Sensor Based on the Magnetostriective Effect,” in 2015 IEEE International Ultrasonics Symposium (IUS), Oct. 2015, pp. 1–3.
[16] M. Elhosni, S. Petit-Watelot, M. Henh, S. Hage-Ali, K. A. Aissa, D. Lacour, A. Talbi, and O. Elmazria, “Experimental study of Multilayer Piezo-magnetic SAW delay line for Magnetic sensor,” in Procedia Engineering, vol. 120, 2015, pp. 870–873.
[17] W. Wang, Y. Jia, X. Liu, Y. Liang, X. Xue, and Z. Du, “Enhanced sensitivity of temperature-compensated saw-based current sensor using the magnetostriective effect,” Smart Materials and Structures, vol. 26, no. 2, pp. 1–10, 2016.
[18] H. Mishra, V. Polewczky, M. Henh, M. Moutaouekkil, C. Floer, K. Dumesnil, D. Lacour, S. P. Watelot, M. Mjahed, S. Hage-Ali, O. Elmazria, N. Tiercelin, Y. Dusch, A. Talbi, and O. B. Matar, “Control of the magnetic response in magnetic field SAW sensors,” Proceedings of IEEE Sensors, pp. 1–3, Oct. 2017.
[19] J. Tong, Y. Jia, W. Wang, Y. Wang, S. Wang, X. Liu, and Y. Lei, “Development of a Magnetostriective FeNi Coated Surface Acoustic Wave Current Sensor,” Applied Sciences, vol. 7, no. 8, pp. 1–16, 2017.
Jean-Michel Friedt obtained his Ph.D. degree in 2000. He worked as a postdoctoral fellow in IMEC, Leuven, Belgium, on acoustic and optical biosensors for characterizing organic thin film properties before joining the group of S. Ballandras in 2004 at FEMTO-ST, Besançon, France, for the development of passive sensors interrogated through a wireless link. He has been an engineer with the company SENSEOR since its creation in 2006, hosted by the Time and Frequency Department of FEMTO-ST. His interests include scanning probe microscopy, passive radio-frequency sensors and the associated radar-like electronics implemented as software-defined radio, and the combination of optical and acoustic methods for characterizing thin films.

Eckhard Quandt received his Diploma and Dr.-Ing. degrees in physics from the Technische Universität Berlin, Germany, in 1986 and 1990, respectively. He is currently a Professor with Kiel University, Kiel, Germany, where he is the Director at the Institute for Materials Science. He is the spokesperson for the DFG CRC 1261 Magnetoelectric Sensors: From Composite Materials to Biomagnetic Diagnostics, and is a member of Acatech, National Academy of Science and Engineering. His scientific focus is material research on smart materials and multiferroics and the development of sensors and actuators for microelectromechanical systems and nanoelectromechanical systems using such materials.

Reinhard Knöchel (M’88-SM’90-F’08-LF’18) received a Dipl.-Ing. degree in electrical engineering and a Dr.-Ing. degree from the Technical University, Braunschweig, Germany, in 1975 and 1980, respectively. From 1980 to 1986, he was a Principal Scientist with the Philips Research Laboratory, Hamburg, Germany. In 1986, he joined the Hamburg University of Technology, where he was a Full Professor of Microwave Electronics until 1993. Between 1993 and 2013, he held the Chair in Microwave Engineering Kiel University, Kiel, Germany. His research interests include magnetic field sensors, active and passive microwave components, ultrawideband technology, microwave measurement techniques, industrial microwave sensors and radar.

Michael Höft (M’04-SM’08) received a Dipl.-Ing. degree in electrical engineering and a Dr.-Ing. degree from the Hamburg University of Technology, Hamburg, Germany, in 1997 and 2002, respectively. From 2002 to 2013, he was with the Communications Laboratory, European Technology Center, Panasonic Industrial Devices Europe GmbH, Lüneburg, Germany. He was a Research Engineer and then a Team Leader, where he was involved in the research and development of microwave circuitry and components, particularly filters for cellular radio communications. From 2010 to 2013, he was also a Group Leader for the research and development of sensor and network devices. Since 2013, he has been a Full Professor at Kiel University, Kiel, Germany, in the Faculty of Engineering, where he is the Head of the Chair of Microwave Engineering of the Institute of Electrical Engineering and Information Technology. His research interests include active and passive microwave components, (sub-) millimeter-wave quasi-optical techniques and circuitry, microwave and field measurement techniques, microwave filters, microwave sensors and magnetic field sensors. He is a member of the European Microwave Association, the Association of German Engineers and a member of the German Institute of Electrical Engineers.