Double phase transition in the triangular antiferromagnet Ba₃CoTa₂O₉

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Abstract

Here, we report the synthesis and magnetic properties of a new triangular lattice antiferromagnet Ba₃CoTa₂O₉. The effective spin of Co²⁺ is found to be \( J = \frac{1}{2} \) at low temperatures due to the combined effect of crystal field and spin–orbit coupling. Ba₃CoTa₂O₉ undergoes two successive magnetic phase transitions at \( T_{\text{N1}} \approx 0.70 \) K and \( T_{\text{N2}} \approx 0.57 \) K in zero applied field, which is typical for triangular antiferromagnets with the easy-axis magnetic anisotropy. With increasing field, the transition anomalies are found to shift toward low temperatures, confirming the antiferromagnetic nature of the transitions. At higher fields, the transition peaks in the heat capacity data disappear and give way to a broad maximum, which can be ascribed to a Schottky anomaly due to the Zeeman splitting of spin levels. The \( H - T \) phase diagram of the compound shows three distinct phases. The possible nature of these phases is discussed.

Keywords: frustrated magnetism, antiferromagnetism, spin–orbit coupling

(Some figures may appear in colour only in the online journal)

1. Introduction

Magnetic frustration and the rich variety of phases driven by competing magnetic couplings have attracted a lot of attention in present-day condensed matter physics [1]. Two dimensional (2D) triangular lattice antiferromagnet (TLAF) is the simplest example of a geometrically frustrated quantum system, where lattice geometry precludes simultaneous minimization of exchange interaction energy on different bonds, thus leading to a highly degenerate classical ground state [2–4]. Quantum fluctuations, which are most pronounced in systems with reduced dimensionality and low spin values, lift the classical degeneracy and stabilize a variety of exotic phases, including quantum spin liquid (QSL) [5–8], spin ice [9], and field-induced states manifesting themselves by plateau features in the magnetization [10, 11]. In a quasi-2D isotropic Heisenberg TLAF, the spins order antiferromagnetically in a 120° structure at zero field. Under external magnetic field this 120° ordered state evolves to an ‘up-up-down’ (uud) state showing a plateau at the 1/3 of the saturation magnetization, through quantum and/or thermal fluctuations, as in the \( S = \frac{1}{2} \) compounds Cs₂CuBr₄ and Ba₃CoSb₂O₉ [12–14]. At very high fields, the uud state becomes unstable leading to canted spin states. Ground states of TLAFs are also sensitive to inter-layer coupling and exchange anisotropy which often lead to even more complex phases [3, 15].

Recently, a family of TLAFs, \( \text{Ba}_3\text{MM}_2\text{O}_9 \) (\( \text{M} = \text{Co, Ni, Cu, Mn and M'} = \text{Sb and Nb} \)), has been studied extensively. These studies unveiled a plethora of interesting properties [14, 16–24]. The \( S = \frac{1}{2} \) compound Ba₃CuSb₂O₉ shows features of a QSL, such as the absence of magnetic long-range ordering (LRO) down to 0.2 K despite the large Curie–Weiss temperature \( \theta_{\text{CW}} \), and the linear temperature dependence of the heat capacity at low temperatures [20]. Owing to the octahedral crystal field and the spin–orbit coupling, the Co²⁺ ion in Ba₃CoSb₂O₉ and Ba₃CoNb₂O₉ features an effective spin \( S = \frac{1}{2} \) at low temperatures. While Ba₃CoNb₂O₉ shows two consecutive phase transitions, Ba₃CoSb₂O₉ has only one transition in zero field, likely due to the easy-axis and easy-plane type anisotropies, respectively [16, 23]. Ba₃CoSb₂O₉ is reported to display magnetization plateaus at intermediate fields below the saturation field [14]. Because of such non-trivial and exotic properties, Co²⁺ based TLAFs are paid a great deal of attention both experimentally and theoretically.
In this paper, we report the magnetic behavior of a new compound of this family, Ba$_3$CoTa$_2$O$_9$. It crystallizes in a hexagonal structure with the space group $\bar{Pm}31$. Figure 1 shows the crystal structure of Ba$_3$CoTa$_2$O$_9$, which can be represented as a framework consisting of CoO$_6$ octahedra sharing corners with dimers of TaO$_6$ octahedra. The Co$^{2+}$ ions, which occupy the $1b$ site, form triangular lattices parallel to the $ab$ plane (see the bottom panel of figure 1) and are separated by non-magnetic Ba atoms. A weak inter-layer coupling still can be envisaged via an extended Co$^{2+}$–O$^{2-}$–Ta$^{5+}$–O$^{2-}$–Co$^{2+}$ pathway. Our magnetic measurements reveal two magnetic phase transitions at $T_{N1} \approx 0.70$ K and $T_{N2} \approx 0.57$ K with a complex $H - T$ phase diagram.

2. Experimental details

Polycrystalline sample of Ba$_3$CoTa$_2$O$_9$ was prepared by a conventional solid-state reaction technique using BaCO$_3$ (99.999%, Aldrich), CoO (99.99%, Aldrich), and Ta$_2$O$_5$ (99.99%, Aldrich) as starting materials. Stoichiometric mixture of the starting materials was intimately ground, pressed into pellets, and fired at 900 °C for 8 h and then at 1200 °C for 48 h in air with intermediate grindings and pelletizations. Phase purity of the sample was confirmed by recording powder x-ray diffraction (XRD) pattern using the PANalytical powder diffractometer (CuK$_\alpha$ radiation, $\lambda_{ave} = 1.5406$ Å) at room temperature. Le-bail fit of the observed XRD pattern was performed using FULLPROF package [26] for which the initial parameters were taken from [25]. Figure 2 shows the room temperature powder XRD pattern for Ba$_3$CoTa$_2$O$_9$ along with its Le-bail fit. All the peaks in the XRD pattern could be indexed based on the space group $P\bar{3}m1$ (No. 164). The lattice parameters obtained from the Le-bail fit [$a = b = 5.7748(6)$ Å and $c = 7.0908(1)$ Å] are comparable to the previous report [$a = b = 5.7750$ Å and $c = 7.0960$ Å] [25]. The goodness of fit parameter was obtained to be $\chi^2 \approx 4.58$.

Magnetization ($M$) measurements were performed as a function of temperature $T$ and applied field $H$ using vibrating sample magnetometer (VSM) attachment to the physical property measurement system (PPMS, Quantum Design). Heat capacity $C_p$ as a function of $T$ and $H$ was measured on a pressed pellet using the relaxation technique in a PPMS. The low temperature ($T \leq 2$ K) $C_p$ measurements were carried out using an additional $^3$He attachment.

3. Results and discussion

3.1. Magnetization

Temperature-dependent magnetic susceptibility $\chi(T)$ ($\equiv M/H$) measured at applied fields of $H = 0.5$ T, 1 T, and 3 T are shown in the upper panel of figure 3. With decreasing $T$, $\chi(T)$ increases in a Curie–Weiss (CW) manner as expected in the paramagnetic regime. No indication of a magnetic LRO was observed down to 2 K. As shown in the lower panel of figure 3, $1/\chi$ varies linearly with $T$ in the high-$T$ regime and a change of slope is observed at low temperatures. In order to extract the magnetic parameters, $\chi(T)$ measured at $H = 1$ T in the high-$T$ regime was fitted by the following expression:

$$\chi(T) = \chi_0 + \frac{C}{(T + \theta_{cw})},$$

where $\chi_0$ is the temperature-independent contribution consisting of core diamagnetism of the core electron shells.
From this value of $\theta$ it develops a curvature, which is more $T$, which corresponds to the $cm^3 mol^{-1}$ $K^{-1}$ would be expected. The reduction in $B$ in $Ba_3CoTa_2O_9$ [14]. Above $()$/$Co$, which is reminiscent of an effective spin-1/2 ground state is also reported for other TLAFs with the octahedral coordinates $Co^{2+}$ sites, such as $Ba_2CoM_2O_6$ ($M = Sb, Nb$) [22, 23] and $ACoB_3$ ($A = Cs, Rb$ and $B = Cl, Br$) [28].

To obtain further insight into the ground-state properties, we measured $M(H)$ isotherms at different temperatures $T = 2.1$ K, $5$ K, $10$ K, and $50$ K, as shown in figure 4. At higher temperatures $T > 50$ K, $M$ varies almost linearly with $H$, as expected for AFM materials with a large exchange coupling. For $T < 50$ K, it develops a curvature, which is more pronounced at low temperatures. At $T = 2.1$ K, the $Co^{2+}$ spins saturate at $H_s \approx 3$ T, above which $M$ increases linearly, but with a much smaller slope.

The inset of figure 4 shows the magnetic isotherm ($M$ versus $H$) and its derivative $dM/dH$ versus $H$ at $T = 2.1$ K in the left and right $y$-axes, respectively. The derivative shows a gradual change of slope with increasing field, and above $\sim 3$ T the change is almost negligible suggesting that the saturation field $H_s$ is close to $3$ T. This small value of $H_s$ is comparable to that reported for $Ba_3CoNb_2O_9$ [17] also reported for the TLAF compound $Ba_3CoNb_2O_9$ [17]. Above $H_s$, there is a slow linear increase in $M$, usually attributed to the temperature-independent Van–Vleck paramagnetic contribution, typical for a $Co^{2+}$ ion in an octahedral environment [29, 30]. Similar scenario is also reported for $Ba_3CoNb_2O_9$ and $Ba_3CoSb_2O_9$ [14, 17, 27]. A linear fit of the data above $H_s$ gives a slope of $\sim 6.4 \times 10^{-2} \mu_B$ T$^{-1}$, which corresponds to the Van–Vleck susceptibility $\chi_{VV} \approx 3.7 \times 10^{-2}$ cm$^3$ mol$^{-1}$. This is in close agreement with the value $\chi_{VV} \approx 3.4 \times 10^{-2}$ cm$^3$ $mol^{-1}$ reported for the TLAF compound $Ba_3CoNb_2O_9$ [17]. From the intercept of the linear fit above $H_s$ on the $y$-axis, the saturation magnetization was obtained as $M_s \approx 1.55 \mu_B$. This value of $M_s (M_s = gJ\mu_B)$ corresponds to an average $g$ value of $g \approx 3.1$ for $J = 1/2$, and the deviation from the free-electron $g$-value of $2.0$ is due to the spin–orbit coupling. Such a large value of $g$ is also reported for $Ba_3CoNb_2O_9$ and $Ba_3CoSb_2O_9$ [14, 17]. The high and anisotropic $g$-values are expected for

(\chi_{core}) and Van–Vleck paramagnetism ($\chi_{VV}$) of the open shells of the $Co^{2+}$ ions present in the sample. The second term in equation (1) is the CW law with the CW temperature ($\theta_{CW}$) and Curie constant $C = N_\Lambda \mu^2_{eff}/3k_B,$ where $N_\Lambda$ is Avogadro’s number, $k_B$ is Boltzmann constant, $\mu_{eff} = g\sqrt{S(S + 1)}\mu_B$ is the effective magnetic moment, $g$ is the Landé $g$-factor, and $S$ is the spin quantum number.

Our CW fit in the high-temperature range ($T > 65$ K) yields $\chi_0 \approx -6.91 \times 10^{-4}$ cm$^3$ mol$^{-1}$, $C \approx 3.96$ cm$^3$ K mol$^{-1}$, and $\theta_{CW} \approx 50.1$ K. From this value of $C$, the effective moment was calculated to be $\mu_{eff} = g\sqrt{S(S + 1)}\mu_B$, expected for the high-spin state ($S = 3/2$) of $Co^{2+}$ taking $g \approx 3.1$, obtained from the magnetization data (discussed later). Since a change in slope was observed at low temperatures for $1/\chi$, the data were fitted separately using equation (1) for $T < 20$ K, which yields $\chi_0 = 0.0355$ cm$^3$ mol$^{-1}$, $C \approx 1.2$ cm$^3$ K mol$^{-1}$, and $\theta_{CW} \approx 1$ K. From this value of $C$, the effective moment was calculated to be $\mu_{eff} \approx 3.1 \mu_B$/Co, which is reminiscent of an effective $S = 3/2$ state with the same $g \approx 3.1$ (the value of $\mu_{eff} = 2.7 \mu_B$ would be expected). The reduction in $\mu_{eff}$ upon cooling is indeed expected for $Co^{2+}$ in the octahedral environment, because spin–orbit coupling $\lambda$ splits the lowest orbital triplet into six Kramers doublets. When the temperature is low enough such that $T < \lambda/k_B$, magnetic behavior is determined by the lowest Kramers doublet with $J = 1/2$, where $J$ stands for the full angular momentum, as opposed to the spin
Figure 5. $C_{\text{mag}}/T$ (left y-axis) and $S_{\text{mag}}$ (right y-axis) as a function of $T$ in the low temperature regime. The downward arrows indicate the two transition anomalies. The horizontal dashed line corresponds to $R \ln 2$. Inset: temperature-dependent heat capacity $C_p(T)$ of Ba$_3$CoTa$_2$O$_9$ measured at zero applied field along with the calculated $C_{ph}(T)$ (solid line).

Co$^{2+}$ compounds in the octahedral environment due to the large orbital contribution [31]. The ESR experiment on the analogous compound Ba$_3$CoSb$_2$O$_9$ indeed reports the high values of $g \approx 3.84$ (for $H|ab$) and $g \approx 3.87$ (for $H|c$) [14].

In contrast to Ba$_3$CoNb$_2$O$_9$ and Ba$_3$CoSb$_2$O$_9$, the anomaly in the $M$ versus $H$ curve at $H_s \approx 3$ T is not very sharp [14, 17]. The shape of this anomaly depends on various factors such as the $g$-tensor anisotropy. In powder samples, this anisotropy smears the anomaly out. Therefore, the fact that our $M$ versus $H$ curve does not show any sharp anomaly at $H_s$ is possibly indicating an anisotropic $g$-value.

3.2. Heat capacity

Heat capacity $C_p(T)$ for magnetic insulators has two major contributions: phononic ($C_{ph}$) and magnetic ($C_{mag}$) parts. At high temperatures, $C_p(T)$ is mainly dominated by $C_{ph}$, while at low temperatures it is mostly of magnetic origin. In order to estimate the phonon part of the heat capacity, the $C_p(T)$ data at high temperature were fitted by the sum of Debye functions

$$C_{ph}(T) = 9R \sum_{n=1}^{4} c_n \left( \frac{T}{\theta_{Dn}} \right)^3 \int_0^{\theta_{Dn}/T} x^4 e^{-x} \left( e^x - 1 \right)^2 dx,$$

where $\theta_{Dn}$ are the characteristic Debye temperatures and $c_n$ are the integer coefficients indicating the contributions of different atoms (or group of atoms) to $C_p(T)$. Similar procedure has been adopted in various other compounds to estimate the phonon contribution [32, 33]. The inset of figure 5 shows $C_p$ data as a function of $T$ in zero applied field and the fit (solid line) by equation (2) with $c_1 = 3$, $c_2 = 1$, $c_3 = 2$, and $c_4 = 9$. Here, $c_1$, $c_2$, $c_3$, and $c_4$ represent the number of Ba, Co, Ta, and O atoms per formula unit, respectively. The sum of $c_n$ equals to 15, which is the number of atoms per formula unit. Because of the large differences in the atomic masses, we used three different Debye temperatures: $\theta_{D1}$ for Ba$^{2+}$ and Ta$^{5+}$, $\theta_{D2}$ for Co$^{2+}$, and $\theta_{D3}$ for O$^{2-}$. Finally, the high-$T$ fit was extrapolated down to 2 K and $C_{mag}(T)$ was estimated by subtracting $C_{ph}(T)$ from $C_p(T)$. $C_{mag}(T)/T$ is plotted as a function of $T$ in figure 5.

To cross-check the reliability of the fitting procedure, we calculated the total magnetic entropy ($S_{mag}$) by integrating $C_{mag}(T)/T$ between 2.1 K and high temperatures as

$$S_{mag}(T) = \int_{2.1 K}^{T} \frac{C_{mag}(T)}{T} dT.$$

(3)

The obtained $S_{mag}$ is plotted on the right y-axis of figure 5. It reaches the value of $S_{mag} \approx 5.1$ J mol$^{-1}$ K$^{-1}$ at around 16 K. This value is only slightly smaller than the expected theoretical value $S_{mag} = R \ln(2J + 1)$ of 5.76 J mol$^{-1}$ K$^{-1}$ for $J = 1/2$. This indeed is a strong evidence for the formation of the $J = 1/2$ state at low temperatures.

The $C_p(T)$ measured at different applied fields from 0 T to 1.5 T in the low temperature regime is shown in the upper panel of figure 6. In zero field, it exhibits two anomalies suggesting two successive magnetic transitions at $T_{N1} \approx 0.70$ K and $T_{N2} \approx 0.57$ K. Below $T_{N2}$, the $C_p(T)$ data were fitted using a power law $C_p \propto T^\alpha$ with the exponent $\alpha \approx 2.05$ (inset of the upper panel of figure 6). A quadratic temperature dependence of $C_p$ in the ordered state is expected for 2D lattices [34]. With increasing field, the transition peaks get smeared and shift towards lower temperatures before they completely disappear at $H \geq 1.5$ T. With increasing field, a broad feature appears at about $T = 2$ K for $H = 1.5$ T, which can be identified as the Schottky anomaly arising due to the Zeeman splitting of the $J = 1/2$ energy levels at low temperatures (lower panel of figure 6). As the field increases, the Schottky anomaly is observed to shift towards higher temperatures. It is to be
noted that, although the peak positions and their heights at the magnetic transition as well as Schottky anomaly regimes are changing with magnetic field, the value of \( S_{\text{mag}} \) at 16 K remains close to 5.76 J mol\(^{-1}\) K, irrespective of the magnitude of the applied field. For \( H = 2 \) T, a theoretical curve was simulated using the Schottky expression,

\[
C_{\text{Sch}} = N \alpha k_B \left( \frac{g \mu_B H}{2 k_B T} \right) \frac{1}{\cosh^2(g \mu_B H/2 k_B T)}. \tag{4}
\]

This expression represents the Schottky specific heat due to the Zeeman splitting of the \( J = 1/2 \) state without exchange interactions between the spins. As shown in figure 6, the low temperature data match well with the simulated curve with \( g \approx 3.1 \), further confirming the large value of \( g \) inferred from the magnetization measurements. The deviations between the simulated curve and experimental data at higher temperatures are attributed to the phonon contribution of the heat capacity.

### 4. Discussion

\( \text{Ba}_3\text{CoTa}_2\text{O}_9 \) shows two successive magnetic phase transitions at low temperatures. It has been theoretically predicted that double magnetic transitions can occur in TLAFs when the magnetic anisotropy is of the easy-axis type, while a single transition is expected for easy-plane type anisotropy [35, 36]. In TLAFs with the easy-axis anisotropy, the 120° state is often preceded by a collinear state. Our zero-field measurements show two transitions that can be thus associated with the collinear state. The narrow intermediate phase \( (\sim 0.18) \) seen in \( \text{Ba}_3\text{CoTa}_2\text{O}_9 \) suggests that the easy-axis anisotropy is significantly smaller than the intra-layer coupling.

The \( H \rightarrow T \) phase diagram derived from the field-dependent \( C_p(T) \) measurements is shown in figure 7. It exhibits three distinct phases denoted by I, II, and III. Region III corresponds to the paramagnetic phase, while regions II and I are expected to be the collinear and 120° spin states, respectively, in line with the theoretical predictions and the subsequent experimental realizations in \( \text{Ba}_3\text{CoNb}_2\text{O}_9 \) and \( \text{RbMn(MoO}_4)_3 \) [17, 37, 42, 43].

The data points in figure 7 are fitted by a power law,

\[
H = H_c (1 - \frac{T}{T_N})^{\beta}, \tag{5}
\]

where the critical field \( H_c \), \( T_N \), and critical exponent \( \beta \) are the fitting parameters. The \( \beta \) value reflects the universality class and dimensionality of the spin system. The values obtained for \( T_N \) are consistent with the transition temperatures at zero applied field and the value of \( \beta \approx 0.31 \) (for \( T_{N2} \)) and 0.38 (for \( T_{N3} \)) are close to the value of \( \beta = 1/3 \) predicted by the mean-field theory for three dimensional (3D) spin systems [44].

### 5. Conclusion

Magnetic properties of the triangular antiferromagnet \( \text{Ba}_3\text{CoTa}_2\text{O}_9 \) were investigated. At low temperatures, it undergoes two successive AFM transitions at \( T_{N1} \approx 0.70 \) K and \( T_{N2} \approx 0.57 \) K with a narrow intermediate phase, which is due to weak easy-axis magnetic anisotropy. \( \text{Co}^{2+} \) adopts the \( J = 1/2 \) state at low temperatures, whereas at higher temperatures the \( S = 3/2 \) state is observed. The magnetization saturates already at \( H_c \approx 3 \) T suggesting weak magnetic interactions in the system. The \( H \rightarrow T \) phase diagram deduced from the heat capacity measurements shows three distinct phases. The above peculiar features render \( \text{Ba}_3\text{CoTa}_2\text{O}_9 \) a model TLAF compound for further experimental and theoretical studies.

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