LETTER

A Modified AdaBoost Algorithm with New Discrimination Features for High-Resolution SAR Targets Recognition

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SUMMARY In this paper, we first propose ten new discrimination features of SAR images in the moving and stationary target acquisition and recognition (MSTAR) database. The Ada_MCBoost algorithm is then proposed to classify multiclass SAR targets. In the new algorithm, we introduce a novel large-margin loss function to design a multiclass classifier directly instead of decomposing the multiclass problem into a set of binary ones through the error-correcting output codes (ECOC) method. Finally, experiments show that the new features are helpful for SAR targets discrimination; the new algorithm had better recognition performance than three other contrast methods.

key words: synthetic aperture radar (SAR), automatic target recognition (ATR), adaptive boosting, high-resolution

1. Introduction

The ability to detect targets, discriminate targets and recognize targets on day/night has long made radar systems a key sensor in many military and civilian applications. As an important aspect of SAR application, SAR automatic target recognition (ATR) has gained increased attention over the last two decades by the radar automatic target recognition (RATR) community [1]. The first step in a typical SAR ATR system is detection, with the purpose of selecting the potential region of interest (ROI). Then, in the discrimination phase, the ROI is processed to remove the clutter false alarms (CFA) and output more accurate target clips. Feature extraction, a key step, can reduce the dimensionality of image chips greatly, extract the effective discrimination features and improve the recognition efficiency. The extracted features are expected to have the properties of effectiveness, robustness and feasibility with tolerable computational complexity. Two approaches are generally employed: select the features from the existing features and extract new features. Finally, targets are recognized by the classifiers according to the features’ combination.

Generally, feature extraction methods are categorized as either linear and nonlinear. Principal component analysis (PCA) and linear discrimination analysis (LDA) [2] are two linear methods. Nonlinear methods included the kernel method and the manifold learning method, such as support vector machine (SVM) [3] and locally linear embedding (LLE) [4]. Concerning Boost, the literature reported many success of Boost algorithm for pattern recognition, including Ada_Boost, Logit_Boost, Grad_Boost and Taylor_Boost [5]. All of these are effective techniques for combining multiple weak classifiers to produce a highly accurate ensemble classifier.

In this paper, we use a novel loss function for the Ada_Boost algorithm to accomplish the multiclass recognition problem directly, instead of decomposing the multiclass into a set of binary ones by the error correcting output codes (ECOC) method [6]. The result of the method will converge to a global optimum and has an exponential decrease of the training error upper bound with the increase of the iteration number. Moreover, we extract ten new features that reflect the contrast difference between the target area and CFA for target discrimination. Extensive experiments on the MSTAR database show that the performance of our method outperforms the other methods in SAR target recognition, when utilizing the new features in combination with the existing features.

2. Features for Target Discrimination

In our approach, the images in MSTAR database are represented by two types of features; we named them as the new features and the classical features. Before the extraction of new features, the classical features should be selected first to obtain the useful discriminatory features of target. The targets in the MSTAR database have the randomly distributed poses; eliminating variations of the target pose can significantly reduce the classification error. Therefore, the first feature we selected is the pose of the targets through pose estimation method used in [7]. For majority of the SAR images, the pose estimation error is within ±5°. The other existing features are selected, 10 features from [8] and 12 features from [9].

To make the feature set as complete as possible, we proposed some new features to help the target discrimination. The SAR images with randomly distributed pose, equivalently, there exist rotation of target in the images. Although we have the pose estimation, the error still exists. In image processing, the geometric invariant moments (GIM) can be represented as important characters of the object, they have the invariant properties of rotational, translational and scale, we can use these features as the target discrimi-
nation features. From the pixels in ROI, the following new features were extracted.

Assume that in the ROI area $D$, the grayscale distribution is $f(x, y)$, $(x, y) \in D$, and the grayscale out of the area $D$ is zero. Respectively, the $p + q$ order origin moments and central moments are defined as:

$$m_{pq} = \sum_{y=1}^{N} \sum_{x=1}^{M} x^p y^q f(x, y)p, q = 0, 1, 2 \ldots$$  (1)

$$\mu_{pq} = \sum_{y=1}^{N} \sum_{x=1}^{M} (x - \bar{x})^p(y - \bar{y})^q f(x, y)p, q = 0, 1, 2 \ldots$$  (2)

Where $N$ and $M$ are the height and width of ROI and $\bar{x} = \frac{\sum_{y=1}^{N} \sum_{x=1}^{M} x f(x, y)}{\sum_{y=1}^{N} \sum_{x=1}^{M} f(x, y)}$. So the normalized center moment is defined as:

$$\eta_{pq} = \frac{\mu_{pq}}{\mu_{00}}$$  (3)

Where $r = \frac{p+q+2}{2}, p + q = 2, 3, \ldots$. Then, use the above define, we can build the following seven GIM features.

$$f_1 = \eta_{20} + \eta_{02}$$  (4)

$$f_2 = (\eta_{20} + \eta_{02})^2 + 4\eta_{11}$$  (5)

$$f_3 = (\eta_{30} - 3\eta_{12})^2 + (3\eta_{21} - \eta_{03})^2$$  (6)

$$f_4 = (\eta_{30} + \eta_{12})^2 + (\eta_{21} + \eta_{03})^2$$  (7)

$$f_5 = (\eta_{30} - \eta_{12})\eta_{30} + \eta_{12}((\eta_{30} + \eta_{12})^2 - 3\eta_{21} - \eta_{03})^2 + (3\eta_{30} + \eta_{03})^2$$  (8)

$$f_6 = (\eta_{30} - \eta_{02})(\eta_{30} + \eta_{12})^2 - (\eta_{21} + \eta_{03})^2 + 4\eta_{11}$$  (9)

$$f_7 = (3\eta_{21} + \eta_{03})(\eta_{30} + \eta_{12})((\eta_{30} + \eta_{12})^2 - 3\eta_{21} - \eta_{03})^2 + (\eta_{30} - 3\eta_{12})(\eta_{21} + \eta_{03})$$  (10)

Seven GIM features can keep the translation, scaling and rotation invariance if the ROI is continuous, they are the famous Hu moments in the image processing field. The last three features are the affine invariant moments (AIM), which are the rotational invaria of ROI. They are defined as follows.

$$f_8 = (\eta_{20}\eta_{02} - \eta_{11}^2)/\eta_{00}^2$$  (11)

$$f_9 = (\eta_{20}\eta_{02} - 6\eta_{30}\eta_{12}\eta_{12} + 4\eta_{30}\eta_{11} - 4\eta_{32}^2)/\eta_{00}^2$$  (12)

$$f_{10} = (\eta_{20}(\eta_{30}\eta_{02} - \eta_{11}^2) - \eta_{11}(\eta_{30}\eta_{02} - \eta_{11})\eta_{02}(\eta_{30}\eta_{11} - \eta_{12}^2))/\eta_{00}^2$$  (13)

All the ten new features and the selected 23 classical features are used in experiments in Sect. 4.

### 3. Modified Adaptive Boost Algorithm

Existing boost algorithms for multiclass classification mainly focus on linear combination of weak learners, which may be insufficient to produce an accurate classifier. In this section, an adaptive multiclass boost algorithm that can learn a more complicated combination of weak learners is presented in detail.

Let assume that the labeled dataset be denoted as $(X, C) = \{(x_1, c_1), \ldots, (x_n, c_n)\}$, $x_i \in \mathbb{R}^d, c_i \in \{1, \ldots, k\}$ denotes the class label, the data $x_i$ are independently and identically distributed (IID), so the objective function is to learn an optimal mapping $f(x) : X \rightarrow \{1, \ldots, k\}$ from the training dataset and a class label $c$ can be assigned to a new input $x$. Note, in the binary classification, the class labels are ±1. However, in the multiclass classification, we need to recode the class label $c$ into a vector $y$, usually, a set of $k$ distinct unit words $Y = \{y_1, \ldots, y_k\}$ were built and each class label $k$ can be mapped into a codeword $y_k \in \mathbb{R}^{k-1}$ to identify the class label. Let $f(x) \in \mathbb{R}^{k-1}$ be a classifier, the margin of $f(x)$ with respect to class $k$ can be defined as following like in [5], [10].

$$F(x) = \arg \max_k \langle f(x), y_k \rangle = \langle f(x), y_k \rangle$$

$$= \langle f(x), y_k \rangle - \max_{l \neq k} \langle f(x), y_l \rangle / 2$$  (14)

Where $< a, b >$ denotes the inner product of a and $b$. therefore, $F(x)$ can find a class which has the largest margin for the classifier $f(x)$, and then we just need to find a optimal classifier $f(x)$ with minimizes the classification risk below.

$$R_L(f(x)) = \mathbb{E}_{x,y}[L(y, f(x))] \approx \sum_{i=1}^{N} \mathbb{L}(y^i, f(x_i))$$  (15)

Where $L(a, b)$ is a multiclass loss function, we define it as $L(y, f(x)) = \sum_{i=1}^{K} \log[1 + \exp(-< f(x), y_i >)]$. In the general boost algorithm the optimal classifier $f(x)$ is approximated as a linear combination of weak learners, that is to say, $f(x)$ is one kind of the linear combinations of weak learners $q_j(x) : X \rightarrow \mathbb{R}^{k-1}$, but in this paper, we use a more complicated combination: the sum of Schur product $\Omega_Q = \{p(x)/p(x) = \sum_j q_{j1}(x) \otimes \ldots \otimes q_{jm}(x), q \in Q\}$, where the $\otimes$ denotes the Schur product, $Q = \{q_1(x), \ldots, q_m(x)\}$ is the set of all multiclass weak learners $q(x) : X \rightarrow \mathbb{R}^{k-1}$. It easy to prove that the functional space $\Omega_Q$ is a convex set, so the following optimization problem is a convex optimization problem and the risk can achieve the global minimum.

$$\begin{cases} \min_{f(x)} R_L(f(x)) \\ s.t. f(x) \in \Omega_Q \end{cases}$$  (16)

After $t$ iterations, the classifier $f(x)$ is assumed to be the form of $f'(x) = \sum_{j=1}^{S} p_{j}(x)$, $S$ is the number of Schur product of $q(x)$, we define $p_j(x)$ as the form in Eq.(17).

$$p_j(x) = q_{j1}(x) \otimes \ldots \otimes q_{jm}(x), m_j \in N$$  (17)

In the iteration process of the boost algorithm, each term can be updated by a new weak learner, $p_j(x) = p_j(x) \otimes q(x)$, so
the updated classifier can be achieved.

\[
f^{t+1}(x) = \sum_{i,j} p_i^j(x) + p_i^j(x) \otimes q(x)
\]

(18)

Where \( \Theta_j^2(x)=\Theta_j^1(x) - p_j^2(x) \), around the point \( \Theta_j^1(x) \), the first and second order functional derivatives of the risk \( R_L(f^{t+1}(x)) \) with respect to the above update in \( f^t(x) \) are

\[
\delta R_L(f^t; q_j) = \frac{\partial R_L(\Theta_j^1(x)+\epsilon p_j^1(x) \otimes q(x))}{\partial \epsilon}
\]

(19)

\[
O_i = \sum_{k=1}^{K} (p_j^1(x) \otimes (y_i - y_k^j))^1 + \exp(-<Q^j(x_i),y_i-y_k^j>)
\]

(20)

\[
\Phi_{t,k} = \frac{\exp(-<Q^j(x_i),y_i-y_k^j>)}{1 + \exp(-<Q^j(x_i),y_i-y_k^j>)^2}
\]

(22)

To each \( j \), using the gradient descent method, there also can use the Newton method as the optimization strategy; in the algorithm we use the gradient descent method. The former brings the greatest decrease of the risk, we can obtain the best weak learner with Eq. (19) and Eq. (21). Moreover, we can obtain the optimal step size as Eq. (24).

\[
q_j^* = \arg \min_{q \in \mathcal{Q}} \delta R_L(f^t(x); q(x))
\]

(23)

\[
\alpha_j^* = \arg \min_{a \in \mathcal{R}} R_L(Q_i^t + a \Phi_j^t \odot q_j^*)
\]

(24)

Hence, the updated classifier has the following risk

\[
R_L(f^{t+1}) = R_L(Q_i^t + a_j^* p_j^1 \otimes q_j^*)
\]

(25)

During each of the iteration, we calculate the optimal multiclass weak classifier, the risk and the direction which brings the greatest decrease of the classification risk [5]. The algorithm is summarized in Table 1 in brevity, we named it Ada_McBoost.

### 4. Experimental Results

In this paper, we use the SAR images in the MSTAR public release database, with 128 × 128 pixels and 1 × 1 foot resolution, to evaluate the performance of the proposed algorithm. Here, the task is to classify three distinct types of ground vehicles: BMP2s (sn-9596, sn-9566, and sn-c21), BTR70 (sn-c71) and T72s (sn-132, sn-821, and sn-s7). Every image has a different poses, which covers from the 0° to 360° aspect range randomly. The depression angles of the images are 15° and 17°. We put the SAR images at the depression angle of 17° in the training dataset and the depression angle of 15° in the testing dataset. Table 2 list the types and the size included in training and testing datasets. All the original SAR images have been preprocessed as following steps. 1) Eliminate the interference of background clutters and target shadow, obtain the ROI. 2) Use the ROI to define the binary mask matrices of the images and extract the target of SAR images by masking the binary matrices and re-center the location of the target. 3) Normalize the energy of images in the same range and execute the gray enhancement of the SAR images based on the power function. At last, we extract the classical features mentioned in Sect. 2 and the new features we proposed to compose the training and testing datasets. Before the feature extraction, each SAR image’s size is cut to 64 × 64 pixels. In order to demonstrate the effectiveness of our proposed algorithm, we compare our algorithm with three other methods (KPCA, KLDA and NGCSE) [11]. The kernel function of KPCA and KLDA is the radial basis function (RBF), in NGCSE, we set the parameters of \( k_1 = 10, k_2 = 20 \), in this situation the algorithm can gets the best performance as discussed in the literature [11], set the maximum number of iterations of Ada_McBoost, conservatively, to 50, from our experience, approximately 20 iteration steps are enough to yield a sufficiently accurate classifier. The confuse matrix is shown in Table 3 and the best accuracy (Bal with the new features,

| Table 1 | Ada_McBoost algorithm |
| --- | --- |
| **Input:** dataset \((X, C)\), the number of classes \(K\), a set of \(K\) distinct unit codewords \(Y\), multiclass loss function \(L(a, b)\), and the number of iterations \(T\). |
| **Output:** \(f(x) = \arg \max_k \frac{\frac{\partial}{\partial \beta} f(x) \odot (x_\beta > 0)}{\sum_k \frac{\partial}{\partial \beta} f(x) \odot (x_\beta > 0)}\) |
| **Algorithm:** |
| Initialization: set \( t = 0 \), \( S = 0 \), and \( f^0(x) = 0 \). |
| Do |
| For \( j = 1 \) to \( S \) |
| Find the greatest decrease direction of the risk \( q_j^* \) by using the method used in [10] through the Eq. (19) and Eq. (21). Then use the Eq. (24) to get the optimal step size \( a_j^* \). Compute the update risk \( R_L(f^{t+1}(x)) \) via Eq. (25). |
| end |
| Set \( j = \arg \min_k R_L(f^{t+1}(x)) \), \( j \in \{0, \ldots, S\} \) and then calculate |
| \( p_j^{t+1}(x) = a_j^* p_j(x) \odot q_j^*(x) \) |
| If \( j \neq j \) update \( p_j^{t+1}(x) \leftarrow p_j(x) \) |
| Update \( f^{t+1}(x) \leftarrow \sum_{j=0}^{S} p_j^{t+1}(x) \) and \( t \leftarrow t + 1 \). |
| While \( t < T \) |

| Table 2 | Summary of MSTAR database |
| --- | --- |
| **Training Set** | **Testing Set** |
| Serial Number | Size | Serial Number | Size |
| --- | --- | --- | --- |
| BTR70 | sn-c71 | 233 | sn-c71 | 196 |
| BMP2 | sn-9563 | 233 | sn-9563 | 195 |
| sn-c71 | 232 | sn-c71 | 196 |
| T72 | sn-132 | 232 | sn-132 | 196 |
| sn-812 | 231 | sn-812 | 195 |
| sn-s7 | 228 | sn-s7 | 191 |
large-margin loss function to solve the convex optimization problem and design the multiclass classifier directly, the Schur product of the weak learners replaces the linear combination of weak learners perfectly. Experiments on the MSTAR dataset demonstrate the effectiveness of our proposed method.

Acknowledgements

This work is supported partly by Postdoctoral Research Fund Plan of Jiangsu province under Grants 1302027C and 2014 innovation project of Jiangsu province KYLX_0369. In addition, the authors wish to thank the anonymous reviewers and editors for their valuable comments and suggestions.

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