The spatial structure of a nonlinear receptive field

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Understanding a sensory system implies the ability to predict responses to a variety of inputs from a common model. In the retina, this includes predicting how the integration of signals across visual space shapes the outputs of retinal ganglion cells. Existing models of this process generalize poorly to predict responses to new stimuli. This failure arises in part from properties of the ganglion cell response that are not well captured by standard receptive-field mapping techniques: nonlinear spatial integration and fine-scale heterogeneities in spatial sampling. Here we characterize a ganglion cell’s spatial receptive field using a mechanistic model based on measurements of the physiological properties and connectivity of only the primary excitatory circuitry of the retina. The resulting simplified circuit model successfully predicts ganglion-cell responses to a variety of spatial patterns and thus provides a direct correspondence between circuit connectivity and retinal output.

Spatial structure in light inputs is conveyed from the photoreceptors to the inner retina where it is sampled by the dendrites of the retinal ganglion cells (RGCs), the output cells of the retina. Empirical models dominate our quantitative characterization of this spatial integration process. Such models have been refined over the past several decades and in many cases can accurately describe responses to the same stimuli to which the models are fit1–3. No models for spatial integration, however, accurately predict the responses of individual RGCs across a wide range of spatial inputs. Further, empirical models by design do not provide a detailed basis for spatial sensitivity in terms of anatomical and physiological features of the retinal circuitry.

Two features of spatial integration in RGCs present major obstacles for a predictive model: nonlinearity and fine-scale heterogeneity. Cat RGCs have been classified based on whether they linearly (‘X’ cells) or nonlinearly (‘Y’ cells) integrate inputs across space4; RGCs showing nonlinear spatial integration have since been identified in many species5–8. Standard approaches to mapping receptive fields, such as those based on spike-triggered averaging, do not capture nonlinear spatial integration. Bipolar cells had been initially proposed9,10 and then demonstrated11 to be the substrate for nonlinear subunits in the RGC receptive field. A remaining challenge is to determine which types of bipolar cell provide input to a given type of RGC and how the sampling of these bipolar cell inputs shapes RGC sensitivity.

Heterogeneity in spatial sampling among individual RGCs of the same type also represents a major obstacle for predictive models. RGC receptive fields exhibit large-scale structure that deviates from either circular or elliptical Gaussian profiles12. Heterogeneities on a finer scale have been measured as ‘hot spots’ in the receptive field that are unique for each RGC13–16. The authors of a previous study had measured fine-scale heterogeneity in the receptive fields of rabbit RGCs but did not find a clear correspondence between hot spots in the receptive field and dendritic patterns of individual RGCs15. The authors had proposed that incorporating information about connectivity between bipolar cells and RGCs might clarify such a correspondence.

A predictive model of the spatial integration of RGCs would have broad implications for understanding retinal circuits. A model based directly on anatomical and physiological mechanisms would by necessity incorporate some aspects of the retinal circuitry and neglect others; a successful model would thus identify aspects of the circuit that are essential to characterize and how they shape spatial sensitivity. Such a model would also help explain how spatial integration changes as the circuitry shaping the responses changes, for example, as signals shift from the rod bipolar to cone bipolar circuits with increasing light levels. Finally, a successful predictive model would be a powerful tool with which to explore computationally how populations of RGCs encode the enormous space of visual patterns.

RESULTS

Nonlinear and heterogeneous spatial integration

We studied a distinct functional and morphological cell type in mouse retina that is identified by its large soma, large and sparse dendrites and high-contrast sensitivity (characterized previously as the G10 RGC by its morphology and neuronal coupling pattern17 and referred to below as the ‘On alpha-like’ RGC18,19). We mapped the linear receptive fields of these cells using standard white-noise stimuli (Fig. 1a–c). Consistent with results from other RGC types and in other species, the spatial profile of the receptive-field center contained hot spots that were not well fit by a two-dimensional Gaussian profile13–16 (Fig. 1b). Also consistent with data for other RGCs5–9, responses to temporally modulated stimuli showed clear evidence for nonlinear spatial integration: spatially uniform stimuli elicited a response dominated by the modulation frequency, whereas temporal modulation of light and dark bars elicited a response at twice the modulation frequency (Fig. 1d).

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Such ‘frequency doubling’ is a hallmark of nonlinear spatial integration\(^{10}\). The frequency-doubled response reached a peak for gratings with a spatial scale of ~40 \(\mu m\) and declined substantially only when the spatial scale exceeded the ~300 \(\mu m\) RGC receptive-field center, presumably stimulating the receptive-field surround (Fig. 1e).

The stimuli and analyses illustrated in Figure 1 and related studies highlight that RGCs do not integrate space linearly or smoothly. These approaches, however, provide incomplete information about alternative models of receptive fields because approaches based on measuring responses to white noise typically assume linear spatial integration\(^{10,11}\), and grating stimuli enable the characterization of sensitivity to spatial scale but not position in two dimensions. Thus we turned to stimuli and analyses that probed heterogeneity and nonlinearity more effectively. In particular, we studied responses to random textures (stimulus construction is described in Online Methods).

As expected from the grating responses (Fig. 1d,e), nonlinear spatial integration was apparent in responses to texture stimuli that had structure on a fine spatial scale but little or no structure on the scale of the entire receptive-field center (Fig. 2a). Cells responded robustly to these texture patterns with a dependence on spatial scale similar to that observed with grating stimuli (Fig. 2b). Such structure is expected from a receptive field composed of nonlinear subunits but cannot be explained by a global nonlinearity applied after linear spatial integration (for example, in standard linear–nonlinear receptive-field models)\(^{11}\).

To probe fine-scale heterogeneity in the spatial sensitivity profiles of individual RGCs, we measured responses to three variants of these texture stimuli: a change in the random seed used to construct the texture (Fig. 2c), small translations of the texture (Fig. 2d) and rotations of the texture (Fig. 2e). These stimuli should produce little or no response modulation if they are perfectly centered on a receptive field that integrates over space with radial symmetry. This lack of response modulation holds true for receptive fields constructed from linear or nonlinear subunits. On alpha-like RGCs, however, were sensitive to all three manipulations, with unique response profiles for each cell (Fig. 2c–e). Errors in the centering of the stimulus with respect to the RGC dendrites, which typically were less than 30 \(\mu m\), could not account for the differences we observed (Supplementary Fig. 1). This sensitivity
bipolar cells provide majority of excitatory input
The unique response profiles of On alpha-like RGCs could be shaped by the sparse pattern of the ganglion cell’s dendrites and their connectivity with the bipolar cell mosaic, as suggested previously\(^1,2\). To test this proposal, we first determined which bipolar cell types dominate excitatory input to On alpha-like RGCs and then characterized both the properties of the excitatory input these cells provide and their connectivity with the RGC dendrites.

RGCs receive input from a subset of bipolar cell types in part owing to the specific stratification patterns of bipolar-cell axon terminals and RGC dendrites\(^22,23\). Can a single bipolar cell type provide the substrate for nonlinear subunits? To answer this question, we first measured the fraction of the excitatory synapses on the RGC dendrites made by type 6 bipolar cells, which make many synaptic contacts with On alpha-like ganglion cells\(^24\).

We identified synapses between type 6 bipolar cells and On alpha-like RGC dendrites by combining biolistic techniques with transgenic labeling of cells. We labeled retinas with four distinct markers (Fig. 4a–f). We biolistically transfected RGCs with cDNA encoding a red fluorescent protein (tdTomato) to visualize their dendrites and a tagged postsynaptic density protein (PSD95-CFP) to label excitatory postsynaptic sites\(^24\). All On bipolar cells expressed YFP in the Grm6-YFP transgenic mouse line\(^25\), and type 6 bipolar cells were labeled by Synaptogamin-2 (Sty2) immunostaining\(^22\). We identified On alpha-like RGCs by their large somata and dendritic morphology. The quadruple labeling allowed us to determine whether each postsynaptic site on the RGC was opposed to an On bipolar cell (Fig. 4c), and if so, whether that bipolar cell was type 6 (Fig. 4d,e and Supplementary Movie 1). Putative synapses with type 6 bipolar cells were distributed evenly throughout the dendritic tree of the ganglion cell and across experiments represented ~70% of the identified inputs from On bipolar cells (Fig. 4f and Supplementary Table 1). Owing to the dim and somewhat patchy nature of the Sty2 label, we likely missed some contacts with type 6 bipolar cells in our analysis. This percentage, therefore, is a lower bound on the proportion of type 6 bipolar cell inputs. An independent measurement of the proportion of type 6 bipolar cell inputs gave a similar result (Online Methods).

Type 7 bipolar cells have also been observed to make synaptic contacts with the On alpha-like RGC\(^25\), so we repeated the synapse-counting experiments in a transgenic line with most type 7 bipolar cells labeled\(^22,26\) (Fig. 4g–j and Supplementary Movie 2). Although particular type 7 bipolar cells often made multiple synaptic contacts with the RGC dendrites, consistent with previous results\(^24\), the majority of type 7 bipolar cells did not make any synapses with the On alpha-like RGC. Across experiments, type 7 bipolar cells accounted for less than 5% of the identified excitatory synaptic sites on the RGC (Supplementary Table 2 and Supplementary Movie 2).

Type 6 bipolar cells constitute nonlinear subunits
The numerical predominance of type 6 bipolar cell inputs to the On alpha-like RGC suggests that they provide the anatomical substrate for nonlinear subunits. To test this suggestion, we quantified the spatial scale of nonlinear interactions in the RGC receptive field and contained in the spikes and that contained in the excitatory input were not distinguishable when measured from the same cells (Fig. 3d). These results indicate that sensitivity to texture rotation is dominated by changes in an RGC’s excitatory synaptic input, with little contribution from inhibitory inputs or intrinsic properties. Thus we focused on identifying the bipolar cell type(s) that provide excitatory input to On alpha-like RGCs.

Excitatory input dominates nonlinear spatial integration
How closely does the receptive field reflect the excitatory synaptic input provided by bipolar cells? To answer this question we compared the excitatory inputs and spike outputs of the same On alpha-like RGC in response to a rotated texture (Fig. 3). The response patterns were nearly identical (Fig. 3c; \(r^2 = 0.97 \pm 0.005\), mean ± s.e.m., 4 cells).

We also characterized sensitivity of RGC responses to rotation angle using linear Fisher information, a measure that defines the error bound of an optimal linear decoder (Online Methods). The information

Figure 3
Excitatory inputs and spike responses have similar sensitivity to rotation. (a) Average firing rate and excitatory input current measured from the same cell in response to a texture stimulus presented at two different rotation angles. Gray bars indicate texture presentation. (b) Spike count (top) and charge transfer in excitatory input currents (bottom) at each rotation angle for the cell in a. Error bars, s.d. across 10 trials at each rotation angle. (c) Normalized spike count versus normalized charge transfer of excitatory input current in response to rotations of a texture stimulus (n = 4 cells 32 total angles). Dashed line is unity. (d) Maximum linear Fisher information about rotation angle across different texture scales for spike counts or charge transfer (Online Methods). Dashed lines connect points from the same cell.
determined whether these spatial nonlinearities were aligned with the locations of type 6 bipolar cells. We quantified nonlinear interactions between two locations in space by measuring responses to small spots of light presented either individually or simultaneously (Fig. 5). Two spatial locations interacted nonlinearly if the response to the spots presented simultaneously differed from the linear sum of the responses to the spots presented individually; we quantified the strength of such nonlinear interactions with a nonlinearity index that measured the deviation from linearity in units of the s.d. of the responses (Online Methods). As inputs to the RGC dendrites should be integrated linearly or near linearly under voltage clamp, we attribute nonlinearities in the measured currents to the synaptic output of the bipolar cell. We observed nonlinear interactions most frequently for spots presented nearby with the average nonlinearity index falling near zero, indicating a linear interaction, when spots were 50–60 μm apart (Fig. 5e). This spatial scale is similar to the spatial scales characteristic of the frequency-doubled response (Fig. 1e) and of responses to random textures (Fig. 2b).

In the experiments described above we characterized the spatial extent of the nonlinear subunits but did not test the role of type 6 bipolar cells specifically. Hence we recorded excitatory inputs in response to light stimuli targeted to individual type 6 bipolar cells using a mouse (Grm6:tdTomato) in which a subset of On bipolar cells is brightly labeled27 (Fig. 5a–d and Online Methods). If the targeted type 6 bipolar cell indeed constituted a nonlinear subunit, we would expect to see a larger nonlinear interaction between a pair of spots presented in its receptive field than between a pair of spots presented across the boundary of its receptive field (Fig. 5f). Indeed, the nonlinearity index was significantly larger for two spots located within a circular region with a radius of 19–25 μm centered on the bipolar cell dendrites than it was for spots located across this boundary (P < 0.01 across this range; Fig. 5g,h). The radius accounting for the most significant effect was 22 μm (P < 0.001; Fig. 5h,i), consistent with both the interaction distance between spots (Fig. 5e) and direct measurements of the bipolar cell receptive field28 (see below). Experimental uncertainties are likely to obscure, rather than inappropriately create, such a correspondence between bipolar cell location and nonlinear interaction strength. For example, some fraction of the many unlabeled bipolar cells could have receptive fields containing the pair of spots, causing scatter in the measured relationship between bipolar cell position and nonlinear interaction between spots. Uncertainty about spot location on the retina or tilt in the photoreceptor array would also blur this relationship. Thus, the actual correspondence
Two physiological properties of subunits of bipolar cells completed the model (Fig. 7a). First, we measured the receptive field of type 6 bipolar cells from their responses to narrow bars of light (Fig. 7b). The dependence of the integrated current on bar position was well described by a circular Gaussian profile (2 s.d. width of 44 ± 8 μm, mean ± s.e.m.; n = 5; Fig. 7b). This is considerably larger than expected from the ~15 μm diameter of the bipolar cell dendrites, but is consistent with the only other measurements of mouse cone bipolar cell receptive fields. The relatively large receptive field likely reflects spread of signals through the gap junctions coupling cone bipolar cells to AII amacrine cells. The receptive-field size of the bipolar cell was fixed in the model. Second, we measured the nonlinearity in a ganglion cell's excitatory inputs by stimulating the entire receptive-field center with uniform 300-μm discs at several contrasts. These large stimuli should uniformly stimulate the population of bipolar cells that provide input to the RGC. We normalized the integrated current at each contrast to the maximum to construct
Figure 6 Construction of the bipolar cell weight map from anatomical measurements. (a) Image of RGC dendrites (blue), PSD95-YFP (green) and type 6 bipolar cell (red). Putative synapses between the bipolar cell and RGC were counted as in Figure 3. (b) RGC dendrites were traced and the length of dendrite in the convex polygonal axonal territory of the bipolar cell axon terminal was measured (thin white lines). (c) Number of putative synapses as a function of RGC dendritic length in the bipolar cell axon territory (n = 28 bipolar cell–RGC pairs; raw data from ref. 27). Dashed line indicates best fit line through the origin (slope = 0.39 synapses µm⁻¹). (d) Histogram of the bipolar cell axon area (mean = 227 ± 51 µm²). (e) Model of bipolar cell weights based on the anatomical measurements in c and d. Tracing of RGC dendrites (green) and model of bipolar cell synaptic weights. Model bipolar cells with nonzero weights are outlined in black, and darker fill colors correspond to larger weights (Online Methods).

The contrast-response function of the excitatory inputs (Fig. 7c). This function is a measure of the average nonlinear transformation occurring between light stimuli and the RGC excitatory input. We generated the full receptive-field model (Fig. 7a) by combining the map of bipolar cell to RGC connectivity modeled for each recorded RGC as in Figure 6e with the spatial sampling (Fig. 7b) and nonlinearity characteristics (Fig. 7c) of type 6 bipolar cells. The model was entirely constrained by the measurements described above with the only free parameter being normalization of the overall response. The only visual stimulus used to construct the model for a particular RGC was a uniform disc used to measure the contrast-response function. Thus, spatial structure in the responses predicted by the model emerges from the bipolar cell receptive field, the anatomical estimate of bipolar cell connectivity based on the RGC dendrites and parameters of the synaptic contacts made by type 6 bipolar cells. Nonetheless, the model generated accurate predictions of stimuli with two-dimensional spatial structure, for example, the response profile of a ganglion cell across the 8 different rotation angles of the texture stimulus (Fig. 7d). The model predictions generalized to other spatial stimuli as well (see predictions for random textures in Supplementary Fig. 4).

Performance of the model was evaluated by comparing the measured responses to a null prediction generated using a different random rotating texture as model input (Online Methods). Across a population of cells, the log-likelihood ratio (base 10) between the model prediction for the appropriate versus null rotating texture was 85 ± 26 (± s.e.m.; n = 10); that is, the model prediction was ~10⁸⁵ times more likely than the null model.

The model in Figure 7 is based on anatomical estimates of the weights of bipolar cell inputs to ganglion cells. Bipolar cell weights could also be estimated physiologically by generating a grid of bipolar cell positions, as in Figure 6e, and assigning a weight to each...

Figure 7 A predictive model of RGC responses to two-dimensional patterns of light. (a) Schematic of the model (Online Methods). The stimulus is sampled by the receptive field of each bipolar cell subunit (see b). The resulting input is passed through the nonlinear output function of the bipolar cell (see c). The bipolar cell outputs are each weighted by the anatomical model and summed at the RGC. (b) Measurement of the receptive field of a type 6 bipolar cell in one dimension. Charge transfer in response to 0.5 s steps of a bright bar (top) at different positions were fit by a one-dimensional Gaussian (bottom). (c) Contrast-response function measurement. Uniform 300 µm discs of light were presented to the RGC while excitatory input currents were measured. The charge transfer, normalized to its maximum, is plotted as a function of the contrast of the stimulus. (d) Response profiles of two RGCs to a texture stimulus at different rotation angles along with model predictions based on the measured nonlinear transfer function and imaged dendrites of each cell. Texture scale was 36 µm. Data points are charge transfer, normalized to the mean, of RGC excitatory input currents. Error bars, s.d. across 10 trials at each rotation angle. The model prediction was calculated for each degree of rotation. Solid purple line is the mean and shaded region is the s.d. over 10 choices of random seed in the jittering of the bipolar cell grid (Online Methods).
bipolar cell based on a fine-scale receptive field (for example, Fig. 1a). Although the bipolar cell weights in such a model are estimated using white noise, the model constructed using these weights differs from a standard linear receptive field because the bipolar cell subunits each provide nonlinear input to the ganglion cell with a nonlinearity measured as above. This physiological approach to estimate bipolar cell weights, however, resulted in substantially poorer predictions than the model based on anatomical weights (by a factor of $10^{6.5}$ for the example cell in Supplementary Fig. 5). This failure could arise from inherent difficulty in characterizing spatial nonlinearities using white-noise approaches and/or the hundreds of bipolar weights that need to be estimated. A previous study has found that receptive fields measured at high resolution with white noise captured gross features of dendritic morphology (as in Fig. 1a) but did not correlate strongly with fine dendritic structure. It remains possible that bipolar cell weights derived from a receptive-field map with higher resolution and lower noise or those derived from a different spatial stimulus could improve model performance to match or exceed that of models based on the anatomically defined weights. The question of how to estimate nonlinear bipolar weights from a physiological measurement is an important area of future research.

Factors contributing to prediction accuracy
What factors determine the accuracy of the model predictions? To answer this question we constructed a set of alternative models (Fig. 8). To explore the role of fine-scale heterogeneity in bipolar cell weights (Fig. 6), we compared predictions of the anatomical-weights model with those of models based on a Gaussian distribution of bipolar weights (Fig. 8a). To explore the role of nonlinear spatial integration, we compared models with linear and nonlinear bipolar cell output functions (Fig. 8a).

Gaussian receptive-field models are often motivated anatomically assuming a constant density of inputs per unit length of RGC dendrite (for example, Fig. 6c) and the increasing sparseness of more distal RGC dendrites. In these models, the Gaussian receptive field originates from a decrease in the number of synapses with distance from the soma resulting from decreasing dendritic coverage, whereas the strength of individual synaptic contacts is assumed constant or near-constant across the dendritic tree. Assumptions that provide the basis for such Gaussian models have been confirmed by anatomical studies. Such models do not incorporate fine-scale dendritic structure but instead assume it is accounted for by the Gaussian falloff in input weights with radial distance. Similar to past models, we generated a Gaussian model by assigning each cell in the simulated mosaic of type 6 bipolar cells a weight based on its distance from the center of mass of the RGC dendrites. Otherwise, we computed the predictions from this model identically to those from the anatomical-weights model described in Figure 7.

Both the fine-scale heterogeneity and nonlinearity of the anatomical-weights model were critical as models with substitutions in either factor did not predict the measured response profile. The Gaussian model generated a slowly varying and periodic dependence on rotation angle owing to imperfect alignment of the stimulus on the bipolar weights (Fig. 8b,c). With a perfectly centered stimulus, the Gaussian model predicted no dependence on rotation angle (Fig. 8b,c). Across 80 rotating-texture responses from ten cells, the anatomical-weights model outperformed the Gaussian model (likelihood ratio; Online Methods) by a factor of $10^{133}$ (Fig. 8c). We describe additional tests of the importance of spatial features of the model in Supplementary Discussion.
Nonlinear transfer at the bipolar cell output was also critical to the performance of the model. As expected for a stimulus with matching distributions of light intensity above and below the background, models with a linear bipolar cell output function averaged zero response across texture patterns (Fig. 8d,e) with predictions too far from the data to define a meaningful likelihood ratio ($>10^{600}$). Such behavior cannot be ‘fixed’ by a single global nonlinearity, as in linear–nonlinear or related models; a global nonlinearity would elevate all responses equally, including the response in the absence of a stimulus altogether. The precise shape of the bipolar cell output nonlinearity was relatively unimportant as a model with a simple rectification in place of the measured nonlinearity performed worse than the model with the measured nonlinearity by only a factor of 12.1 across the population (data not shown).

**DISCUSSION**

Here we showed that responses of individual RGCs to arbitrary spatial patterns can be predicted using the measured properties of the bipolar cell inputs to an RGC: size of the receptive field, connectivity pattern with the RGC and output nonlinearity. Predictions of this mechanistically based model were much more accurate than empirical models for spatial selectivity. The model describes how spatial sensitivity depends on connectivity between bipolar cells and ganglion cells and the physiological properties of the signals RGCs receive from their bipolar-cell inputs.

**Model simplifications and their validity**

Our anatomically based model captured the response profiles of individual RGCs more closely than previous receptive-field models based on linear spatial integration or a Gaussian weighting of nonlinear subunits (Fig. 8). The failure of linear models is expected given the clear nonlinearities in spatial integration exhibited by similar cell types in other species. The failure of Gaussian models indicates that fine structure in the dendrites cannot be captured by a Gaussian falloff in bipolar cell weights with distance from the soma.

Our model, nonetheless, makes considerable simplifications. We neglected bipolar cells other than type 6 ones that make excitatory synapses on the On alpha-like RGC dendrites (Fig. 4). Type 7 bipolar cells provide less than 5% of the excitatory synapses (Fig. 4) and hence are unlikely to have a major role shaping spatial sensitivity. Type 8 bipolar cells, which also stratify with the dendrites of On alpha-like RGCs, have much larger dendritic fields than either type 6 or 7 bipolar cells, so they would be predicted to be less sensitive to texture patterns with fine spatial structure. Based on the similar spatial selectivity of the excitatory synaptic input and spike responses (Fig. 3), the model also neglects presynaptic and postsynaptic inhibition and active properties of the RGC dendrites.

The success of the model in predicting RGC responses to two-dimensional texture patterns (Figs. 7 and 8) indicates that, at least for these stimulus manipulations, the model incorporated (and neglected) an appropriate set of circuit mechanisms. Spatial stimuli of increased complexity, especially those including interactions between space and time, will challenge the predictive power of this simplified model but may highlight the applicability of the anatomically based approach.

With targeted physiological measurements and appropriate anatomical markers, other input circuits could be mapped and layered on top of the primary photoreceptor to bipolar cell to RGC pathway. Even without mapping the additional circuitry, deviations from the type 6 bipolar cell pathway prediction under various stimulus conditions could be used to isolate the functional role of other circuits such as the excitatory input from other bipolar cell types or inhibition either onto the bipolar cell terminals or onto the RGC dendrites.

**Quantitatively relating connectivity and function**

We report to our knowledge the first identification of a particular bipolar cell type that provides the basis for nonlinear subunits in the RGC receptive field and the first quantitative prediction of the fine structure of the RGC receptive field from the connectivity between the bipolar cell mosaic and the RGC dendrites. Most previous studies of RGC receptive fields have used linear systems approaches and thus assumed linear spatial integration by construction (Supplementary Fig. 5c). Models that capture nonlinear spatial integration have used simplifying assumptions about subunit connectivity such as a circular Gaussian profile. Although several groups have speculated about the connection between the dendritic morphology of individual ganglion cells and their spatial receptive fields, they have not established a quantitative link between the two or have concluded that fine dendritic structure has only a weak and unimportant role in determining how the RGC samples visual space.

The proliferation of specific labels for bipolar cell types along with a growing set of data on retinal connectivity will enable subsequent receptive-field models to incorporate connectivity data into quantitative descriptions of RGC function. As researchers studying other visual areas or other sensory systems begin to uncover how inputs are mapped across the dendritic arbor of a neuron, the approach of incorporating detailed connectivity data into functional models could provide a valuable framework.

**Dendritic morphology influences stimulus selectivity**

The sparse dendritic morphology of On alpha-like RGCs led to fine-scale heterogeneity in the weights of bipolar cell inputs (Figs. 6 and 8a) and contributed to their different responses to texture patterns presented at slightly different angles or positions (Fig. 2). Models based on Gaussian weighting of nonlinear subunits will be sensitive to textured stimuli but not to different texture patterns or small movement of a given texture. Indeed, our anatomically defined model was more sensitive to small (15 µm) translations of natural image stimuli than a Gaussian receptive-field model (Supplementary Fig. 3). These considerations suggest that the relative density of RGC dendrites will be a key determinant of selectivity for different spatial features. Indeed, others have found receptive-field hot spots primarily in wide-field ganglion cells and suggested that these cells might respond to different visual features than narrow-field ganglion cells with more dense dendritic arbors.

Fine-scale structure of the receptive field is not beneficial for encoding all classes of stimuli, but instead should be viewed as a parameter that influences what types of visual stimuli are best encoded. A heterogeneous receptive field will create different ambiguities in a cell’s response than a Gaussian receptive field. For example, a small object crossing through the receptive field would create a temporally modulated response owing to the spatial heterogeneity in synaptic weights; a similar response could be produced by temporal modulation of a spatially invariant object. However, a heterogeneous receptive field is more sensitive than a Gaussian receptive field to the position of a small object (Supplementary Fig. 6) or a small translation of a natural image (Supplementary Fig. 3). The vast array of RGC morphologies may offer important clues about their stimulus selectivity. Our anatomically based model of RGC responses could be integrated into future modeling and experimental work aiming to explore the relationship between dendritic morphology and stimulus selectivity.

**Encoding and decoding in a heterogeneous population**

We found that individual RGCs of the same type respond differently to the same stimulus patterns (Fig. 2c–e) based on their unique dendritic
branching patterns. The unique response fingerprint provided by the dendrites, together the extensive dendritic overlap of nearby On alpha-like RGCs, raises several questions about coding in a heterogeneous population. Are the dendrites of neighboring RGCs of the same type positioned in a way that increases correlation between the cells or does independence at a small spatial scale among overlapping dendritic fields allow for more independent encoding of spatial patterns? Is heterogeneity encoded in the encoding of visual patterns by the RGC population, or is it a source of noise, limiting the fidelity of the population code? If RGC selectivity to stimulus features such as texture angle or position does carry useful information, how is the signal decoded in downstream circuits? Although new experiments will be needed to answer these questions, a predictive model of RGC responses will be an important tool for modeling the response of a heterogeneous population.

METHODS

Methods and any associated references are available in the online version of the paper.

Note: Supplementary information is available in the online version of the paper.

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AUTHOR CONTRIBUTIONS

G.W.S. performed ganglion cell recordings, analysis and designed receptive-field models. H.O. performed imaging experiments and analyses (Figs. 4 and 6). F.A.D performed bipolar cell recordings (Fig. 7b). J.L.M. and D.K. performed imaging experiments analyzed in Figure 6. G.W.S., R.O.W. and F.R. conceived of experiments and analyses. G.W.S., H.O., F.A.D., R.O.W. and F.R. wrote the paper.

COMPETING FINANCIAL INTERESTS

The authors declare no competing financial interests.

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ONLINE METHODS

Recording. Tissue preparation and RGC recordings were performed as described previously except that the retina was affixed to a glass slide covered in α-polyl-lysine (BD Biosciences). All animal procedures were approved by the Institutional Animal Care and Use Committee at the University of Washington. Cell-attached recordings with Ames solution in the recording pipette were used to measure spike responses. For whole-cell voltage clamp recordings in RGCs and type 6 bipolars, the internal solution contained 105 mM CsCH3SO3, 10 mM TEA-Cl, 20 mM HEPES, 10 mM EGTA, 5 mM Mg-ATP, 0.5 mM Tris-GTP, 2 mM QX-314 and 0.2 mM Alexa Fluor 488 or Alexa Fluor 750 (pH -7.3 with CsOH, -280 mOsm). RGCs were adapted to the background light level for at least 10 min before data collection, and data were collected only from cells that had stable and robust spike responses to 10% contrast steps.

The small-spot experiments (Fig. 5) were performed in a mouse with sparse labeling of On bipolar cells. A target type 6 bipolar cell was first identified by axon terminal morphology in the two-photon microscope, and its cell body was identified by following the axon. Stimuli were centered on the cell body. Throughout this procedure, laser power was kept low (<4 mW at the sample) to minimize light exposure. A whole-cell voltage clamp measurement was made from a nearby On alpha-like RGC, and the cell was filled with a fluorescent dye. After the recording, the region of retina was imaged at higher power (~10 mW) so that bipolar dendrites were visible. If the axon of the target bipolar was approaced to the RGC dendrites in a single image plane (Fig. 5c), the data were included in the analysis. Alignment of spots was based on the center of mass of the bipolar dendrites in the high-power image (Fig. 5d).

Type 6 bipolar cells were recorded and filled in flat mount retina and identified by morphology and stratification in the inner plexiform layer (IPL) after recordings. We approached the bipolar cells by tearing a hole through the inner limiting membrane and ganglion cell layer ~100 µm lateral from the site of recording and moved the patch pipette diagonally through the IPL to reach the On bipolar cell bodies in the inner nuclear layer.

Visual stimulation. Visual stimuli were displayed on a 800 × 600 pixel OLED array (eMagin) and projected onto the photoreceptors from below. Pixels were either 1.2 or 1.8 µm on the retina. OLED display intensities were calibrated and linearized in software. Throughout stimulation, the retina was illuminated with a uniform background light, b, causing 500–1,500 rhodopsin isomerizations per rod per second. Light intensities, I, in the spatial patterns are described in terms of their contrast defined as

\[
\frac{I - b}{b} \times 100\%
\]

Checkerboard stimuli used to measure the linear receptive field (Fig. 1a,b) consisted of random patterns of 18 µm squares at either -100% or 100% contrast covering the entire monitor and updated at a frame rate of either 15 Hz or 30 Hz. Frequency-doubled responses (Fig. 1e,f) were measured using square waves in space (~80% to 80% contrast) at a variety of bar widths, masked by a 600-µm-diameter circle centered on the recorded cell. The contrast in each pixel within the mask was modulated sinusoidally at 3.75 Hz for 20 cycles per trial.

Texture stimuli were created by convolving a random binary pixel map with a two-dimensional Gaussian filter. The resulting images were cropped by a 300-µm-diameter circular mask and renormalized to contain a uniform distribution of contrasts from -100% to 100%. The mean intensity across the texture equaled that of the surrounding background-only region. The spatial scale of the texture is defined as the 2r width of the Gaussian filter. Textures were presented for 0.5 s with at least 1.5 s between trials. Manipulations of the texture stimulus by changing the rotation angle, center location or random seed are described in Results.

In the single and paired-spot experiments (Fig. 5), spot stimuli were 9 µm in diameter, and presented at 300–2,000% contrast for 100 ms. For measurements of the type 6 bipolar cell receptive field (Fig. 7b), rectangular bars 9 µm × 72 µm at 1,500% contrast were presented for 0.5 s with 1 s between trials. Bar position was varied in steps of 9 µm parallel to the short dimension.

Uniform discs to measure the contrast response function in the input currents to the RGC (Fig. 7c) were 300 µm in diameter, centered on the RGC. They were presented for 0.5 s with 1.5 s between trials at contrasts ranging from -100% to 100%.

A test pattern presented on the stimulus monitor was imaged after each recording to aid in the registration between visual stimuli and fluorescence images.

Analysis. The linear space-time receptive field (Fig. 1a–c) was calculated as the reverse correlation of the spike train with the random checkerboard stimulus in 5 ms bins. The spatial and temporal filters were deconvolved by an iterative procedure. First we computed an initial spatial projection of the receptive field by taking the maximum intensity value in time at each pixel. The following steps were iterated (usually twice): (i) a two-dimensional Gaussian was fit to a spatial projection of the receptive field, (ii) the temporal filter was estimated as the mean time projection for pixels inside the 2r boundary of the spatial Gaussian, and (iii) the spatial projection was recomputed along the estimated temporal filter. Cycle-averaged responses to temporally modulated bars excluded the first cycle in each trial. The power spectrum of the average response was computed, and we reported the power of the frequency-doubled F2 component at 7.5 Hz (Fig. 1e).

Responses to texture patterns were quantified as the spike count for cell-attached recordings, or the charge transfer for whole-cell recordings, during the 0.5 s presentation of the texture corrected for the baseline in the 0.5 s preceding stimulus presentation. To account for time dependent changes over long recordings, response amplitudes were drift corrected by subtracting a baseline obtained from the preceding and subsequent trials. Drift correction did not substantially alter the reported results.

The linear Fisher information, \( I_\theta \), for rotated texture stimuli was as:

\[
I_\theta = \frac{1}{R(\theta)} \frac{d}{d\theta} R(\theta)
\]

where \( R(\theta) \) is the mean response for each rotation angle \( \theta \), and \( C \) is the covariance of the responses across angles.

To assess nonlinear interactions between spot locations (Fig. 5), we quantified the response to each spot presented individually, \( R_a \) and \( R_b \) and the response to the spots presented simultaneously, \( R_{ab} \), as the projection of the current trace on each trial along a template derived from the mean response to the simultaneous presentation. The nonlinearity index, NLI, was computed based on these responses and of the observations of each, \( N \), as follows:

\[
\text{NLI} = \frac{1}{N} \sum_{i=1}^{N} \left( \frac{R_{ab} - R_a - R_b}{\sigma_a \sigma_b} \right)^2
\]

The spot responses by the integrated current gave similar results.

Type 6 bipolar cell responses (Fig. 7b) were quantified by the integrated current during presentation of each bar stimulus. Receptive fields were fit in each dimension by a one-dimensional Gaussian. Circularity of the receptive field was assessed in the two cells for which the receptive field was measured in two directions. In these cells, the mean difference between width in the two dimensions was 33%.

Contrast response functions for an RGC’s excitatory input (Fig. 7c) were quantified by integrating the current measured during the presentation of discs at varying contrasts.

To compare the RGC responses to different rotation angles of a texture, \( D(\theta) \), to the model output, \( M(\theta) \), we first scaled both the data and model to a mean response of unity (Fig. 7: model construction described below). The likelihood of a given model response given the data was calculated as

\[
\ell = \prod_{\theta} \frac{P_D(M(\theta) - D(\theta))}{\sigma_D(\theta)}
\]

where \( P_D \) denotes the Gaussian probability density function. The likelihood of the model when presented with the same stimulus as the cell, \( \ell_{\text{cell}} \), was compared to null prediction, \( \ell_{\text{null}} \), obtained by presenting the model with a texture stimulus with the same statistics as the real stimulus, but a different random seed. We report log likelihood ratios for the comparison of the veridical to null models averaged over 10 null models with different random seeds:

\[
\log_{10} \frac{\ell_{\text{ver}}}{\ell_{\text{null}}}
\]

Cell transfection. RGCs were biolistically transfected as described previously. Briefly, isolated retinas were mounted on nitrocellulose membrane.
filters RGC side up. Gold particles of 1.6 μm diameter were coated with plasmids encoding CFP-tagged PSD95 or tdTomato under the control of the CMV promoter, and delivered to RGCs using a Helios gene gun (Bio-Rad). The retina was then incubated for 24 h in mouse artificial cerebral spinal fluid (119 mM NaCl, 2.5 mM KCl, 1.3 mM MgCl2, 2.5 mM CaCl2, 1 mM NaHPO4, 11 mM glucose and 20 mM HEPES, pH 7.4) in an oxygenated chamber heated at 33 °C. At the end of the incubation, the retina was fixed in 4% (w/v) paraformaldehyde for 20 min and washed in 0.1 M phosphate buffer saline (PBS, pH 7.4).

Immunohistochemistry. Fixed retinas were cryoprotected in PBS with a sucrose gradient (10%, 20% and 30%, w/v), and frozen and thawed twice. The tissue was then incubated in PBS containing mouse monoclonal anti-Syt2 antibody (1:200, znp-1, Zebrafish International Resource Center, University of Oregon, Eugene), 5% normal donkey serum, 0.5% Triton X-100 and 0.05% sodium azide, for 5 at 4 °C. After washing the primary antibody, the tissue was incubated with a donkey anti-mouse IgG DyLight 649 secondary antibody (Jackson ImmunoResearch Laboratories; 715-606-150) overnight at 4 °C. After washing the primary antibody, the tissue was incubated with a donkey anti-mouse IgG DyLight 649 secondary antibody (Jackson ImmunoResearch Laboratories; 715-606-150) overnight at 4 °C.

Imaging. Images of fixed retinas described in Figures 4 and 6 were acquired with Olympus FV1000 confocal microscope using 1.35 NA, ×60 or 1.4 NA, ×60 oil objectives. The voxel size was 0.103 × 0.103 × 0.3 μm for Figure 4, and 0.069 × 0.069 × 0.2 μm for Figure 6. Live images of RGC dendrites along with bipolar cells (Fig. 4) were acquired with a Nikon FN-1 two-photon microscope with 980 nm excitation light using a 1.0 NA, ×60 objective with a voxel size of 0.414 μm × 0.414 μm × 0.350 μm. Images of RGC dendrites for the predictive model (Fig. 6) were acquired either with two-photon illumination at 980 nm using a 0.5 NA, ×20 objective with a voxel size of 1.24 μm × 1.24 μm × 1.00 μm or with one-photon infrared illumination using a 0.25 NA, ×10 objective with a voxel size of 1.55 μm × 1.55 μm × 1.50 μm.

Image analysis. Acquired images were median filtered to remove photomultiplier noise. For the image analysis in Figure 4, all PSD95 puncta in the entire image were identified as described previously using our custom-written program in Matlab (Mathworks). As shown in Supplementary Movies 1 and 2, each identified PSD95 punctum was visually assessed in 3D for potential apposition with the axonal terminals of type 6 bipolar cells24. Type 7 bipolar cell axons were identified as described previously using our custom-written program in Matlab (Mathworks). The intensity of the Syt2 immunoreactivity. The intensity of the Syt2 signal was variable across cells, making it more difficult to judge whether a particular type 6 axon was assigned to the G10 dendrite when the immunolabeling was dim. To circumvent this limitation, we used the Gmis-YFP transgenic mouse line in which all On bipolar cell axons are brightly labeled by expression of YFP25. In this line, even dimly expressing Syt2 axons could be visualized using the YFP signal (Supplementary Movie 1).

For the image analysis in Figure 6, pairs of type 6 bipolar cells and On alpha-like RGCs obtained in a previous study were reanalyzed. We arrived at an independent estimate of the proportion of type 6 bipolar contacts from this analysis. We found that a given G10 RGC has on average 0.5 synapses μm−1 dendrite, so the 0.39 synapses μm−1 dendrite within the type 6 bipolar cell axonal field (Fig. 6c) represent 78% of the synapses assuming complete tiling of type 6 bipolar cell axonal terminals.

Binary masks of bipolar axons and RGC dendrites were created using Amira (Visage Imaging), and projected onto a single z plane to generate polygonal territories of bipolar axon terminals and for skeletonizing RGC dendrites. Numbers of synapses between individual pairs of type 6 bipolar cells and On alpha-like RGCs were obtained from a previous study41.

Bipolar weights model. Model bipolar cell locations were generated as a jittered hexagonal grid. Grid spacing was 16 μm plus gaussian noise (σ = 2 μm), and bipolar axon territories were generated by the Voronoi tessellation of these center positions. Randomization of the bipolar positions was varied as described in the text and legends, but other parameters remained fixed. These parameters were chosen so that the distribution of axon territory areas matched both the mean and s.d. of the measured distribution for type 6 bipolar cells (Fig. 6d).

Images of RGC dendrites were traced by hand. The length of dendrite within the axonal territory of each model bipolar was computed, and the bipolar weight was assigned according to the measured density of 0.39 synapses μm−1 of dendrite (Fig. 6c). Bipolar weights were rounded to the nearest integer, and each bipolar with a nonzero weight was assigned a circular Gaussian receptive field with a 2σ width of 44 μm normalized to integrate to unity.

Construction of anatomical-weights model. A two dimensional stimulus was represented in the model by the contrast in each pixel, S(x,y). The stimulus was scaled and aligned to match the image of the RGC dendrites. The receptive field of each model bipolar, Fb(x,y), was multiplied point by point with the stimulus and summed. For each bipolar, the resulting contrast value

\[ c_b = \sum_{x,y} S(x,y)F_b(x,y) \]

was served as the input to the contrast response function, N(c_b), measured for the RGC (Fig. 6c) and linearly interpolated between the measured points. The resulting bipolar responses were each scaled by the bipolar weight, \( W_b \), as described above and summed to give the final model RGC response, \( M \):

\[ M = \sum_{b=1}^{N_{bipolars}} W_bN(c_b) \]

To account for the unknown angle of shear between the photoreceptors on which stimuli were presented and the imaged RGC dendrites, we allowed the model to vary the assumed stimulus position by up to 25 μm from the position determined by alignment. We chose the stimulus position that maximized the log-likelihood estimate of the model prediction given the measured data. Evidence that this small displacement fitting procedure did not over-fit noise and bias our interpretation of the quality of model fits is given in Supplementary Figure 1.

Alternative models. We tested alternative models by systematically substituting pieces of the nonlinear anatomical-weights model described above with more traditional assumptions about spatial integration (Fig. 8 and Supplementary Fig. 5). These substitutions are described below.

Gaussian bipolar weights. Bipolar weights were derived from a two-dimensional Gaussian distribution centered on the center of mass of the RGC dendrites, with a 2σ width matching the largest distance between dendrites. Each bipolar cell was assigned a weight by the distance between the bipolar center and the center of mass of the RGC dendrites. The weight matrix was normalized so that the sum of bipolar weights matched that of the anatomical-weights model. In the optimized Gaussian model, the fit likelihood was optimized by shifting the stimulus arbitrarily relative to the Gaussian weight profile. Supplementary Table 3 summarizes the differences between the anatomical and Gaussian bipolar weights models.

Receptive field measurement weights model. Each bipolar cell received a weight equal to that of the nearest pixel in a spatial receptive field measured as described above with 18 μm flickering squares. 

Linear. The contrast response function used as an input-output relationship for each bipolar was replaced by a line of unity slope.

51. Abbott, L.F. & Dayan, P. The effect of correlated variability on the accuracy of a population code. Neural Comput. 11, 91–101 (1999).