A fermionic portal to a non-abelian dark sector

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We introduce a new class of renormalizable models for dark matter with a minimal particle content, consisting of a dark SU(2)D gauge sector connected to the standard model through a vector-like fermion mediator, not requiring a Higgs portal, in which a massive vector boson is the dark matter candidate. These models are labeled fermion portal vector dark matter (FPVDM). Multiple realizations are possible, depending on the properties of the vector-like partner and scalar potential. One example is discussed in detail. Fermion portal vector dark matter models have a large number of applications in collider and non-collider experiments, with their phenomenology depending on the mediator sector.

KEYWORDS
dark matter, large Hadron collider, vector-like fermions, dark gauge group, relic density, direct dark matter detection

The nature of DM, whose existence has been established beyond any reasonable doubt by several independent cosmological observations, is one of the greatest puzzles of contemporary particle physics. Models with a vector DM, especially in the non-abelian case, are the least explored but well-motivated, as the gauge principle offers guidance and constraints limiting the possible theoretical constructions (see, e.g., [1–26], for a discussion of non-abelian DM in different setups, in particular using non-renormalizable kinetic mixing terms or Higgs portal scenarios). In this article, we develop a new minimal framework that extends the gauge sector of the standard model (SM) by a new non-abelian gauge group for which no renormalizable kinetic mixing terms or Higgs portal scenarios. In this article, we develop a new minimal framework that extends the gauge sector of the standard model (SM) by a new non-abelian gauge group for which no renormalizable kinetic mixing terms are allowed1 and under which all SM particles are singlets. The full model structure, Lagrangian, and particle content are presented in the following sections, along with the main results and immediate prospects for experimental testing, while more technical details can be found in [27].

The simplest non-abelian group is SU(2), which in the following will be labeled SU(2)D as it connects the SM to the dark sector. The gauge bosons associated with SU(2)D are labeled as $V^D_\mu = (V^D_{\mu\nu}, V^D_{\mu\nu}, V^D_{\mu\nu})$, where, here and in the following, the electric charge is specified in the field superscripts, while the isospin under SU(2)D (D-isospin) is specified in the field subscripts. The covariant derivative associated with SU(2)D is

1 Contributions to gauge kinetic mixing may arise at the loop level, depending on the structure of the Higgs sector, but they correspond to suppressed higher operator terms.
\[ D_\mu = \partial_\mu - \left( \frac{g_D}{\sqrt{2}} v^D T_D + i g_D v^D T_D^\dagger \right), \]

where \( g_D \) is the SU(2)_D coupling constant and \( T_D \) is the D-isospin.

The fields responsible for breaking the gauge symmetries are two scalar doublets:

\[
\Phi_H = \left( \phi^+ \phi^0 \right)^T \sim \langle \Phi_H \rangle = \frac{1}{\sqrt{2}} (0 \ 0 \ v),
\]

\[
\Phi_D = \left( \phi^D_1 \phi^D_2 \right)^T \sim \langle \Phi_D \rangle = \frac{1}{\sqrt{2}} (0 \ 0 \ v D),
\]

where the first is breaking SU(2)_L \times U(1)_Y, while the second is breaking SU(2)_D via their respective vacuum expectation values (VEVs) \( v \) and \( v_D \).

The scalar potential for \( \Phi_H \) and \( \Phi_D \) reads

\[
V(\Phi_H, \Phi_D) = -\mu^2 \Phi_H^T \Phi_H - \mu^2 \Phi_D^T \Phi_D + \lambda (\Phi^T H^* \Phi_H)^2 + \lambda_D (\Phi^T D^* \Phi_D)^2 + \lambda_{\Phi_H \Phi_D} \Phi_H^T \Phi_D^T \Phi_D^T \Phi_H,
\]

which was introduced in [2] and ensures that the gauge bosons of SU(2)_D are degenerate and stable because of the custodial symmetry of the scalar Lagrangian. Although the operator \( \Phi^T_H \Phi_D \Phi_D^* \Phi_H \) is not protected by any symmetry and cannot thus be removed from the potential, coupling \( \lambda_{\Phi_H \Phi_D} \) can have any value. If it is small enough, the dark sector would be effectively decoupled from the SM and only observable through gravitational effects. Moreover, the Higgs portal induces scalar mixing, which modifies Higgs–SM couplings and generates Higgs–DM interactions, all of which are strongly constrained [28]. Here, we suggest a different mechanism of communication between the dark and visible sectors via a fermion doublet \( \Psi = (\psi_D, \psi) \), vector-like (VL) under SU(2)_D, and both elements of which are singlets under SU(2)_L, sharing the same hypercharge as one of the SM right-handed fermions. The mass and Yukawa interaction terms of \( \Psi \) read

\[
-L_f = M_{\Psi} \Psi \Psi + (y^D \Psi D \Phi_H f^{SM}_D + h.c.),
\]

where \( f^{SM}_R \) generically denotes an SM right-handed singlet and \( y^D \) is a new Yukawa coupling connecting the SM fermion with \( y_{\Psi H} = \frac{1}{\sqrt{2}} y_{\Psi H}^D \Psi \Phi_H \) through the SM fermion.

Without this symmetry, such a term would be compulsory since the scalar doublet, \( \Phi_H \), is in the pseudo-real representation. The symmetry-breaking pattern is SU(2)_L \times U(1)_Y \rightarrow U(1)_Y^P.\)

Using U(1)_Y phase assignments \( Y_D = \frac{1}{2} \) for dark doublets and \( Y_D = 0 \) for triplets, there is still an invariance under the subgroup

\[
Z_2 = (-1)^{\Phi_D}, \quad \text{where } Q_D = T_D^3 + Y_D. \quad \text{The new particles are summarized in Table 1.}
\]

The lightest \( Z_2 \)-odd particle is stable and could be either \( V^{0}_D \) or \( \psi_D \) with very different consequences from a cosmological point of view [27]. We consider the case where the lightest \( Z_2 \)-odd particle is \( \psi_D \), which we label fermion portal sector dark matter (FPVDM).

The theory contains six massive gauge bosons (\( Z, W^\pm, V^{0}_D, \) \( V^{0}_D \)), and therefore, six Goldstone bosons correspond to their longitudinal components. The remaining two degrees of freedom correspond to physical scalars, which include the SM Higgs boson and another CP-even scalar. By denoting the neutral scalars in terms of their components in the unitary gauge as \( \phi^0 = \frac{1}{\sqrt{2}} (v + h) \) and \( \phi^{0}_D^\dagger \psi_D + \phi^1_D, \) the mass terms of the scalar Lagrangian reads

\[
L^S_m = \left( h_1 \phi_1 \right) \left( \begin{array}{c} \frac{\lambda^{D} v^D}{2} \left( \lambda D v^D \right) \\ \lambda_{\phi^0_0} v^D \end{array} \right) \left( \begin{array}{c} \phi^0 \end{array} \right) \right) (v_D + \phi_1),
\]

Upon diagonalization, the mass eigenvalues read

\[
m^2_{\phi_{1,2}} = \lambda^{D} v^D + \sqrt{\left( \lambda D v^D \right)^2 + \lambda_{\phi^0_0} v^D \left( \frac{\lambda D v^D}{2} \right)^2},
\]

with the mixing angle \( \theta_\phi = \frac{1}{2} \sqrt{\left( \lambda D v^D \right)^2 + \lambda_{\phi^0_0} v^D \left( \frac{\lambda D v^D}{2} \right)^2} \).

In the fermion sector, the component with \( T_D = +1/2 \) gets only a VL mass; therefore, \( m_{\psi_D} = M_f \). However, the other fermion masses are generated after both scalars acquire a VEV. The fermionic mass Lagrangian reads

\[
L^f' = \left( f^{SM}_L \Psi \phi^0 \right) \left( \begin{array}{c} y^D \sqrt{v^D} M_f \phi^0 \end{array} \right) \frac{v^D}{\sqrt{2}} \left( \begin{array}{c} \phi^0 \end{array} \right) \right) (\frac{\lambda^{D}}{2} v^D + \lambda_{\phi^0_0} v^D \phi^0),
\]

The mass eigenvalues are

\[
m^2_{f,2} = \frac{1}{4} \left[ \Delta \pm \sqrt{\Delta^2 - 8 y^2 v^2 M^2_{f}} \right],
\]

where \( \Delta = y^2 v^2 + y^2 v^2 + 2 M^2_{f} \), \( f \) identifies the SM fermion, and \( F \) identifies its heavier partner. The mass hierarchy is \( m_f < m_{\psi_D} \leq m_Y \).

The Yukawa couplings and mixings can be expressed in terms of the masses of the physical fermions. The new fermion sector is completely decoupled in the limit \( m_f = m_{\psi_D} \), for which \( y = y_{SM} \) and \( y' = 0 \). When the full flavor structure of the SM is taken into consideration, different possibilities can be considered. A VL fermion can interact with one or more SM flavors, and there can

### Table 1: Quantum numbers of the new particles under the electro-weak (EW) and SU(2)_D gauge groups.

| SU(2)_L | U(1)_Y | SU(2)_D | Z_2 |
|---------|--------|---------|------|
| \( \Phi_D \) | \( \psi_D \) | \( \phi^0 \) | \( \phi^1 \) |
| 1 | 0 | 2 | + |
| \( \Psi \) | \( \psi \) | \( \phi^0 \) | \( \phi^1 \) |
| 1 | 0 | 2 | + |
| \( V^{0}_D \) | \( V^{0}_D \) | \( V^{0}_D \) | \( V^{0}_D \) |
| 1 | 0 | 3 | + |

The bold numbers correspond to the representation of the multiplets under SU2.
be multiple VL fermions. The Cabibbo–Kobayashi–Maskawa (CKM) matrix of the SM might also receive contributions from new physics induced by the mixing of SM and VL quarks. The masses of the SM gauge bosons are not altered by the presence of $\Phi_D$. The gauge bosons of $SU(2)_L$ are all degenerate in mass at the tree level: $m_{V_D} \equiv m_{V_D^\pm} = \frac{\mu}{v} \equiv m_{V_D}$. This degeneracy is broken by kinetic mixing in the broken EW and dark gauge symmetry phases and by the different fermionic loop corrections associated with the opposite $\mathbb{Z}_2$ parities of the $SU(2)_D$ gauge bosons. Such different contributions might affect loop corrections to $Z$ and $W$ masses, addressing the CDF anomaly [32]. In the following, to simplify notation, we will label $V_D$ and $V_{D^\pm}$, with mass $m_{V_D}$, and $V' \equiv V_{D^0}$, with mass $m_{V'}$. The leading contribution to the radiative mass split of $V'$ and $V_D$ bosons, $\Delta m_V = m_{V_D} - m_{V'}$, is determined by $F$ and $\psi_D$ loops and reads

$$\Delta m_V = \frac{\epsilon \bar{g}_D^2 m_F^2}{32 \pi^2 m_{\psi_D}} + o(\epsilon^2), \quad \text{where} \quad \epsilon = \frac{m_{V_D}^2 - m_{V'}^2}{m_{V_D}^2}. \quad (9)$$

In the following, we assume that new VL fermions interact only with one flavor of the SM. Six independent input parameters are thus necessary to describe the new physics sector of the model, namely, $g_D$, $m_{V_D}$, $m_{\psi_D} \sin \theta_D$, $m_F$, and $m_{\psi_D}$. Let us now discuss a specific realization of the model, assuming only one VL partner interacting exclusively with the SM top quark and no mixing between $h$ and $H$, i.e., $\theta_D = 0$. This choice significantly simplifies the Lagrangian; the Higgs sector of the SM is not affected by the new physics at the tree level, and the potential of $\Phi_D$ has the very same structure as the Higgs potential. A mixing between $h$ and $H$ is induced only by fermionic loops and will be neglected in the following. Therefore, in this case, the model is described by the following five parameters: $g_D$, $m_{V_D}$, $m_0$, $m_t = m_{\tau}$, and $m_{\psi_D} = m_{\psi_D}$. The hierarchy between the masses in the fermion sector is $m_0 < m_{\psi_D} \leq m_{\tau}$ while $H$ can have any mass allowed by experimental bounds, even being lighter than the SM Higgs boson.

In our study, we tested this realization of the model against multiple observables from cosmology, DM direct, and indirect detection (DD and ID) experiments and LHC searches. For this purpose, the Lagrangian has been implemented in SPheno [33] and Feynrules [34], while model files have been generated in CalcHEP [35], UFO [36], as well as FeynArts [37] formats and are available on the hepforge library [38]. This implementation has been used in micromegas V5.27 [39] for the evaluation of various DM observables and for extracting the respective limits. The model implementation in UFO format has been used in MG5_aMC [40] for the determination of the LHC constraints. Collider simulations have been performed at LHC using the NNPDF3.0 LO set [41] through the LHAPDF6 library [42] (LHA index 262400). A simplified version of the model has been implemented to calculate cross-sections at one loop in MG5_aMC and FORMCALC9.8 [43].

The amount of relic density is determined by the interplay of annihilation and co-annihilation processes, a subset of which is shown in Figure 1A. ID constraints are associated with DM annihilation rates at CMB time, excluding regions of parameter space where the injection into SM-plasma in the early universe is too large to be consistent with CMB data. Both the relic density and ID processes are tested against PLANCK data [44]. DD processes arise from diagrams such as those shown in Figure 1B and are tested against limits from XENON 1T [45]. The LHC bound has been obtained via testing of $t\bar{t}$ pair production with subsequent decay into $V_D$ and top quarks against CMS searches for top squark pair production decaying into DM [46]. The relevant limit from $TT$ of even partners of the SM top quark from the respective ATLAS and CMS searches is approximately 1.5 TeV for $m_{\tau}$ [47, 48]. Single $T$ production is less constrained, as it is driven by the small $T^\pm t$ mixing.

We also estimated the relevance of $V'$ pair production and associate production of $V'$ with the Higgs boson, occurring at LO via fermion loops. Representative topologies for the tested processes are shown in Figure 1C. The complementarity of cosmological and collider constraints has been studied by performing a comprehensive scan over the parameter space (excluding the fixed parameter $\sin \theta_D = 0$) projected onto the $(g_D, m_{V_D})$ plane, as shown in Figure 2. The allowed
The parameter space is indicated by the green, cyan, and blue regions, presenting generic DM annihilation, dominated by the $t$-channel diagram of Figure 1A, resonance ($H$) and DM-$t_0$ co-annihilation regions, respectively, which satisfy the relic density constraint from PLANCK within 5%. The allowed regions of the parameter space are superimposed on top of the forbidden ones to provide their best visualization in this projection of the five-dimensional scan into the two-dimensional plane.

The generic DM annihilation determines a lower limit on $g_D$ as a function of $m_{V_D}$. At the same time, the $H$-resonant region allows for the reduction of $g_D$ values by up to two orders of magnitude, while the strong DM-$t_0$ co-annihilation channel allows for even lower values of $g_D$ for not-so-heavy DM. For $m_{V_D}$ above 2 TeV, however, the co-annihilation mechanism saturates, while $H$-resonant annihilation requires larger $g_D$ coupling for higher DM mass to provide the right amount of relic density. Therefore, the region with $m_{V_D} \geq 1$ TeV has an over-abundant relic density, as indicated by the dark red color, except the space with large values of $g_D$ couplings, corresponding to the bulk $V_D V_D \rightarrow V' V'$ annihilation and $H$-resonant annihilation presented in Figure 2 by green and light-blue colors, respectively. Notice also that the regions with $m_{V_D} \lesssim 1$ TeV values are partly excluded by DD and/or ID experiments, as indicated by magenta and orange points, respectively. The region of DM masses that can be tested and excluded by the LHC is $m_{V_D} \lesssim 400$ GeV, represented by the violet region.

To assess the relative role of the different constraints, we identify representative benchmarks characterized by different gauge couplings, $g_D = 0.05$ and $g_D = 0.95$, and fixed values for the masses, $m_T = 1,600$ GeV and $m_{H} = 1,000$ GeV. For these points, gauge coupling is small enough to allow a perturbative treatment in a region of parameter space, which can be tested by both collider and cosmological observables.

We show in Figure 3 the exclusion regions in the $[m_{V_D}, m_{V_{D}'}]$ and $[m_{V_D}, 1 - m_{V_{D}'}, m_{H}]$ planes to highlight the low $m_{V_D}$ or low $m_{V_{D}'} - m_{V_D}$ regions, respectively. The masses of the DM candidate $V_D$ and mediator $t_0$ are left as free parameters.

The predicted relic density is consistent with PLANCK results only in specific regions: for $g_D = 0.05$ (left and central panels of Figure 3), most of the parameter space predicts an over-abundant relic density, except for an area where the mass difference between $t_0$ and DM is less than $\sim 10\%$ of the mediator mass (where $t_0$-$t_0$ and DM-$t_0$ co-annihilation processes dominate), a small area around $m_{V_D} = m_{H}/2$ (DM annihilation via resonant $H$), and $m_{V_D} \lesssim 10$ GeV. For larger values of $g_D$ (right panel of Figure 3), annihilation processes become more effective, reducing the size of the excluded area in the lower $m_{V_D}$ region and eventually extending the under-abundant relic density region. The enhancement of the $V_D V_D \rightarrow V' V'$ process, due to $\Delta m_{V} > 0$, affects the relic density and ID signals. The complementarity of various constraints is especially evident for small values of $g_D$ in the low $m_{V_D}$ region. The region excluded by ID corresponds to small values of $m_{V_{D}'}$ for $g_D = 0.05$, $m_{V_{D}'} \lesssim 10$ GeV.
largely overlapping with the region excluded by relic density, and rapidly vanishes as $g_2$ increases. The large region excluded by DD is mainly determined by processes (see Figure 1B) with sizable kinetic mixing or DM multipole moment contributions, taking place in the regions with low $m_{\nu_\tau}$ values (i.e., below few hundreds GeV).

The LHC bound is almost independent of the mass of $t_D$ until its mass difference with the DM reaches the top-quark threshold: in that region, $E_{\text{miss}}$ decreases and the sensitivity of the CMS search reduces, allowing a small mass-gap region. As the process is QCD-initiated, the bound is also almost independent of other parameters of the model. Processes of $V'$ pair production and associated production of $V'$ with the Higgs boson would only be potentially testable in a region already excluded by DD constraints (see orange and blue contours in the right panel of Figure 3). The model has an important feature, especially for small values of $g_2$, in the small DM-$t_D$ mass-gap region where the correct relic density is reproduced. In this region, $t_D$ is long-lived (its lifetime in the small mass-gap region is shown in the central panel, Figure 3) and can be probed by dedicated searches at the LHC or future colliders. Different $T$ or $H$ masses would not modify this qualitative picture.

The FPVDM scenario introduced in this paper connects a vectorial DM candidate from a non-abelian $SU(2)_D$ gauge group to the fermionic sector of the SM without the necessity of a Higgs portal at the tree level, and the mechanism is realized in the most economical way, with a minimal set of new parameters and new particles. Even the simplest realization of FPVDM, involving interactions of the dark sector with only one SM fermion, has great potential to explain DM phenomena and has several important implications for collider and non-collider DM searches. Minimal FPVDM realizations involving other SM fermions can be used to explain outstandingly observed anomalies. For example, if the VL fermion interacts with the leptonic sector of the SM, new contributions might explain $g - 2)_\mu$ [49] and, at the same time, provide novel physics cases for future $e^-e^+$ colliders [50–53]. Minimal realizations, including mixing in the scalar sector, further VL partners, or additional interactions of the same VL representation, would open up a vast range of possibilities for future studies, both phenomenological and experimental, and would allow one to explore the complementarity between collider and non-collider observables in multiple scenarios.

**Data availability statement**

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

**Author contributions**

AB: writing—original draft and investigation. LP: writing—original draft and investigation. AD: writing—original draft and investigation. SM: writing—original draft and investigation. DR: writing—original draft and investigation. NT: investigation and writing—original draft.

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**Conflict of interest**

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