Novel excitations near quantum criticality in geometrically frustrated antiferromagnet CsFeCl₃

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The investigation of materials that exhibit quantum phase transition provides valuable insights into fundamental problems in physics. We present neutron scattering under pressure in a triangular-lattice antiferromagnet that has a quantum disorder in the low-pressure phase and a noncollinear structure in the high-pressure phase. The neutron spectrum continuously evolves through critical pressure; a single mode in the disordered state becomes soft with the pressure and it splits into gapless and gapped modes in the ordered phase. Extended spin-wave theory reveals that the longitudinal and transverse fluctuations of spins are hybridized in the modes because of noncollinearity, and previously unidentified magnetic excitations are formed. We report a new hybridization of the phase and amplitude fluctuations of the order parameter near a quantum critical point in a spontaneously symmetry-broken state.

INTRODUCTION

For understanding condensed matter, investigation of collective excitation in the low energy range is indispensable. According to quantum field theory, excitation in a system with spontaneously symmetry breaking is characterized by phase and amplitude fluctuations of order parameters. The former is known as the Nambu-Goldstone (NG) mode, and the latter is called as the amplitude mode. Although these modes are usually separated, they are hybridized under some conditions, and interesting phenomena are induced; for example, in a crystal lattice system, acoustic phonon (NG mode) and optical phonon (amplitude mode) are hybridized through anharmonic terms in a thermoelectric material PbTe, which renormalizes the phonon spectrum and leads to low thermal conductivity and high figure of merit in thermoelectric property (1). Such a hybridization effect could exist in other types of elementary excitations; however, no research has been reported to our knowledge. One of the reasons is that the amplitude mode itself is not trivial in other systems: superconductors (2), charge density wave (3), ultracold atoms (4), and insulating antiferromagnets. The existence of the amplitude mode in the antiferromagnets requires strong fluctuation of the magnetic moment and the system location near a quantum critical point (QCP). So far, it has been found in a number of spin systems free from geometrical frustration such as quasi-one-dimensional chains (5, 6), dimer (7–9), square lattice (10), and two-leg ladder antiferromagnet (11). In magnets, in the presence of geometrical frustration that could induce the hybridization of modes, magnon excitations from ordered states have been less focused these days (12), although fractional excitations in the spin liquid were intensively studied (13–15). In particular, the collective excitations from a noncollinear spin structure in a geometrical frustrated lattice near QCP have not been studied, and its investigation is of primary importance to find a novel state and to advance the physics of the frustration and quantum criticality.

Spin S = 1 easy-plane antiferromagnet is one of the prototypical quantum spin systems that allows exploring the nature of the quantum phase transition (QPT) (16, 17). The Hamiltonian is expressed by $H = \sum_i (D S_i^z S_i^z + J_{ij} (S_i^+ S_j^- + S_i^- S_j^-))$, where $S_i$ is the spin operator at the i site. The first term $D$ is positive and gives an easy-plane single-ion anisotropy. The second term is a Heisenberg interaction with $J_{ij} > 0$ for an antiferromagnetic coupling. The positive $D$ splits the triplet $S = 1$ states into the singlet ground state $S^z = 0$, and the doublet excited states $S^z = \pm 1$.

Fig. 1. Spin $S = 1$ easy-plane antiferromagnet. (A) Schematic diagram of the $S = 1$ easy-plane antiferromagnet. In the ordered state, the doublet excited states $|\pm 1\rangle$ splits into $|L\rangle$ and $|T\rangle$. Here, the former and latter have longitudinal and transverse fluctuations, respectively. (B) Crystal structure of CsFeCl₃ with the space group P6₃/mmc (30). Magnetic Fe²⁺ ions having pseudospin $S = 1$ form one-dimensional chains along the crystallographic c axis, and the chains form the triangular lattice in the ab plane. Red and blue lines indicate the intrachain interaction $J_c$ and interchain/intratriangle interaction $J_{ab}$, respectively.

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Hayashida et al., Sci. Adv. 2019;5:eaaw5639 18 October 2019 1 of 5
and it favors a quantum disordered (QD) state as shown on the left in Fig. 1A. By contrast, the spin interaction $J_{ij}$ allows the system to cause a magnetic long-range order (LRO).

In the LRO phase, the energy eigenstates change as shown on the right in Fig. 1A. Here, $|G\rangle$ is the ground state, while $|T\rangle$ and $|L\rangle$ are excited states. They are given by $|G\rangle = u|0\rangle + v/\sqrt{2}(|1\rangle + |\bar{1}\rangle)$, $|T\rangle = 1/\sqrt{2}(|1\rangle + |\bar{1}\rangle)$, and $|L\rangle = -v|0\rangle + u/\sqrt{2}(|1\rangle + |\bar{1}\rangle)$ with $u^2 + v^2 = 1; u$ and $v$ are determined by $D$ and $J_p$. In the ordered phase, $v \neq 0$ and a finite magnetic moment appears in the $ab$ plane (16, 17). We separate the spin operator into longitudinal ($S^\parallel$) and transverse ($S^\perp$) components relative to the local ordered moment. A remarkable feature is that the second excited state $|L\rangle$ can be excited only by the longitudinal component $S^\parallel$, while the first one $|T\rangle$ can be excited by the transverse component $S^\perp$.

Thus, the excited states at a local site are separated into two states having longitudinal and transverse fluctuations. The studies in the square lattice predicted an enhanced amplitude/longitudinal mode as a one-magnon excitation in addition to the NG/transverse mode in the LRO phase near the QCP (10, 16). In the collinear magnetic structure, in general, the transverse and longitudinal fluctuations are not hybridized, and they are separated (5–11). In the geometrically frustrated spin system, on the other hand, these fluctuations could be hybridized because of the noncollinearity of the magnetic structure. This point was theoretically investigated in the continuum-like spectra in the $S = 1/2$ and $S = 3/2$ systems, where the longitudinal fluctuation stems from two-magnon process (18). Since $S = 1$ easy-plane antiferromagnet has the longitudinal fluctuation in one-magnon process, in contrast, the two fluctuations hybridize in one-magnon level, and a novel excited state may appear as a well-defined eigen mode. Details of such a study, however, have not been reported either in experiment or theory.

CsFeCl$_3$ is a model material for the $S = 1$ easy-plane triangular antiferromagnet as shown in Fig. 1B. The inelastic neutron scattering (INS) study at ambient pressure revealed that the ferromagnetic chains along the $c$ axis are antiferromagnetically coupled in the $ab$ plane (19). The ground state is the QD state because of large single-ion anisotropy. The magnetic susceptibility measurement under pressures exhibited a

![Fig. 2. Inelastic neutron scattering spectra.](http://advances.sciencemag.org/) The spectra obtained at a chopper spectrometer under (A) 0.0 GPa at 6 K, (B) 0.3 GPa at 2.7 K, and (C) 1.4 GPa at 0.9 K sliced by the energy transfer – wave vector (hω – $q$) plane for $q = (-k, 2k, 0)$. The yellow circles, squares, and red diamonds are the peak positions of the excitations obtained from the constant-$q$ scans using a triple-axis spectrometer. The solid yellow curves are the dispersions calculated by ESW. Calculated neutron cross section by the ESW under (D) 0.0 GPa, (E) 0.3 GPa, (F) 1.4 GPa, and (G) 4.0 GPa at 0 K. Calculated neutron cross section in the absence of the cross term in Eq. 2 under (H) 4.0 GPa and (I) 1.4 GPa at 0 K. The black and red solid curves in (F) to (I) are gapless and gapped modes, respectively. More detailed pressure dependence of the calculated spectra is shown in fig. S3.
pressure-induced magnetic order above a critical pressure of about 0.9 GPa (20). Because of the strong easy-plane anisotropy, the ordered moment aligns in the ab plane; the neutron diffraction evidenced the noncollinear 120° structure in the LRO phase (21). CsFeCl₃ is, thus, a promising host for the pressure-induced QPT in the geometrically frustrated lattice.

**RESULTS**

**INS spectra of CsFeCl₃ under hydrostatic pressures**

The INS spectrum measured at 0.0 GPa by using a chopper spectrometer in Fig. 2A exhibits a single dispersive excitation with the energy gap of 0.6 meV at the wave vectors \( q = (-k, 2k, 0) \) for \( k = 1/3 \) and 2/3, which is consistent with a previous report (19). The energy gap at 0.3 GPa in Fig. 2B becomes softened when approaching the ordered state (21). A qualitatively different spectrum is observed in the ordered state at 1.4 GPa in Fig. 2C. A well-defined gapless excitation emerges at \( k = 1/3 \) and 2/3, and another dispersive excitation with the minimum energy transfer (ho) of about 0.55 meV is observed in the higher energy range.

**Detailed structure of INS spectra**

The INS spectra at 1.4 GPa were collected by using a triple-axis spectrometer to cover wide \( \hbar \omega \) to \( q \) range as shown in Fig. 3A. The spectral lineshapes at \( k = 1/3 \) and 2/3 are fitted by double Lorentzians convoluted by experimental resolution functions. The excitation becomes broad at \( k = 5/6 \), where four peaks are expected as shown in Fig. 2C. Because it is difficult to resolve it into four peaks, we used the convoluted double Lorentzians. The extracted peak energies are overplotted in Fig. 2C with red diamonds.

Although the linewidth is large, the extracted dispersion relation and the momentum dependence of the intensity are consistent with the theoretical result, as shown in fig. S5. The details of convolution calculation are described in section S4.

The pressure evolution of the energy gap at \( q = (-1/3, 2/3, 0) \) is shown in Fig. 3B. The excitations at 0.0, 0.3, and 0.6 GPa show that the gap is suppressed with an increase in pressure. At 0.8, 0.9, and 1.1 GPa, the gap position cannot be identified, and the broad excitations are observed below 1.0 meV. This implies that the system is near the QCP at these pressures. At 1.4 GPa, the excitation appears at 0.55 meV, which corresponds to the high energy mode in Fig. 2C. The intensity of the excitation at 1.4 GPa in Fig. 3B is weak compared with those in the QD phase. This is because most of the magnetic intensity is concentrated at the magnetic Bragg peak owing to the LRO.

The energies of the gap at 0.0, 0.3, and 0.6 GPa and the transition temperatures obtained both in the present and previous (21) studies are plotted in Fig. 3C.

**DISCUSSION**

To discuss the obtained spectra, the one-magnon cross section was calculated on the basis of the extended spin-wave (ESW) theory (22). It is equivalent to the harmonic bond-operator theory (23–26), and it is convenient to apply complex spin systems such as noncollinear ordered states (17). For CsFeCl₃, we study the following Hamiltonian

\[
\mathcal{H} = \sum_i S_i^2 + J_{chain} \sum_{\langle i, j \rangle} S_i \cdot S_j + J_{ab} \sum_{\langle i, j \rangle} S_i^\parallel \cdot S_j^\parallel \tag{1}
\]

where the sum is taken over the exchange interactions \( J_c \) and \( J_{ab} \) as shown in Fig. 1B. The relation between the crystallographic axes and the global xyz coordinate of the spin system is shown in Fig. 4A. Here, we focus on the last term and rewrite it as \( \mathcal{H}_{ij}^{ab} = \sum_{mn \neq 0} \mathcal{H}_{ij}^{mn} \sin \theta \sum_{\langle i, j \rangle} \mathcal{H}_{ij}^{ab} \), where \( \mathcal{H}_{ij}^{mn} \) is the Hamiltonian of the ordered state and \( \mathcal{H}_{ij}^{ab} \) is the Hamiltonian of the ordered state with the minimum energy transfer (ho).

Here, \( \phi_{ij} = \phi_i - \phi_j \) and \( \phi_s \) represents the angle of the magnetic moment at the i site. The first two \( (\eta \xi + \zeta \xi) \) terms are diagonal for the \( |L\rangle \) and \( |T\rangle \) states, while the last \( \xi \) term leads to hybridization between the \( |L\rangle \) and \( |T\rangle \) states (LT-hybridization). We will call it LT-hybridization term hereafter. For instance, the \( |T\rangle \) state can move from the j site to the i site and change into the \( |L\rangle \) state (see Fig. 4C). This process is described as \( J_{ab} \sin \phi_i (L | S_i^\parallel \rangle \langle G | S_j^\parallel \rangle |T\rangle a_{ij}^a a_{ij}^a \). In the same way, the pair creation

\[
\mathcal{H}_{ij}^{cd} = J_{ij}^{cd} = J_{ij}^{mn} \sin \theta \sum_{\langle i, j \rangle} \mathcal{H}_{ij}^{ab} |L\rangle \langle G | S_i^\parallel \rangle |T\rangle a_{ij}^a a_{ij}^a.
\]

\[
\sum_{\langle i, j \rangle} \mathcal{H}_{ij}^{ab} = J_{ij}^{ab} = J_{ij}^{mn} \sin \theta \sum_{\langle i, j \rangle} \mathcal{H}_{ij}^{ab} |L\rangle \langle G | S_i^\parallel \rangle |T\rangle a_{ij}^a a_{ij}^a.
\]
process is described as $J_{ab} \sin \varphi_g (L | S_i^0 | G(T) | S_j^F | G) a_i^\dagger a_j^\dagger$. The detailed description of the processes is summarized in fig. S2. We emphasize that one-magnon processes for the LT-hybridization can only exist in non-collinear states, i.e., $\sin \varphi_g \neq 0$ in Eq. 2.

Spin interactions and anisotropy are parametrized by comparing the experiment and calculation, and they are represented as a function of the pressure by the linear-interpolation as follows: $J_c (\text{meV}) = 0.0312 - 0.365 \times p$ and $D (\text{meV}) = 2.345 + 0.365 \times p$, where $p$ (GPa) is the value of pressure. The pressure dependencies of the excitation energies at $q = (1/3, 2/3, 0)$ are indicated by circles and solid curves in Fig. 3D. The data are reasonably reproduced by the calculation within the linear pressure dependence in $J_c$, $J_{ab}$, and $D$. The calculated dispersion relations obtained by using the extracted parameters are indicated by the solid yellow curves in Fig. 2 (A to C), and the calculation is consistent with the experiment both in the QD and LRO phases. Furthermore, the calculated INS spectra in Fig. 2 (D to F) reproduce the observed ones.

To understand the effects of LT-hybridization, we demonstrate the INS spectra after dropping the LT-hybridization term in Eq. 2. The results are shown in Fig. 2 (H and I), where the gapless (gapped) modes are pure transverse (longitudinal) modes in this case. With an increase in pressure from 1.4 to 4.0 GPa, the longitudinal modes shift to the high-energy region and lose intensity, as in the collinear case of TlCuCl₃ (8). When LT-hybridization is taken into account, off-diagonal elements between the $|L\rangle$ and $|T\rangle$ states lead to level repulsion. Far from the QCP ($p = 4.0$ GPa), the INS spectrum is not affected by the hybridization [compare Fig. 2, G and H]. By contrast, the spectrum is strongly renormalized by the hybridization near the QCP [compare Fig. 2, F and I], and novel magnetic excitations are formed: both gapless and gapped modes are accompanied by strong longitudinal and transverse fluctuations. The shape of the INS spectrum resembles that in the QD phase (compare Fig. 2, E and F). Note that the spectrum continuously evolves through the QCP, and the property of the second-order phase transition is ensured by considering LT-hybridization. Thus, LT-hybridization plays an important role in magnon dynamics in noncollinear magnets near QCP. The INS measurements in CsFeCl₃ revealed this by the fine tuning of pressure through the QCP.

Since the newly found excitation exists in a noncollinear spin structure, the search of the excitation in different types of noncollinear structures such as cycloidal structure, all-in all-out structure, and skyrmion lattice would be interesting topics. The search of the hybridized mode in other systems including charge density wave, spin density wave, and ultracold atoms would be important. Last, the effect of hybridization to the lifetime of the magnon and other elementary excitations would be also interesting.

**MATERIALS AND METHODS**

A single crystal sample was grown by the vertical Bridgman method (20). The sample was mounted in a Teflon cell with a deuterated glyc erin as a pressure medium so that the horizontal plane is the $ab$ plane. The Teflon cell was installed in a piston-cylinder clamped cell made of CuBe alloy. We performed the INS study under pressure using a high-resolution chopper (HRC) spectrometer at J-PARC/MLF in Japan (27–29) and a cold neutron triple-axis spectrometer CTAX at Oak Ridge National Laboratory (ORNL) in USA. The details of the experimental setups including the name of the spectrometer, sample mass, applied pressure, the energy of the neutron, and the temperature are summarized in table S1.

In the HRC experiment, the pressure cell was installed into the closed-cycle $^4$He cryostat for 0.0 and 0.3 GPa and the $^3$He cryostat for 1.4 GPa. The energies of the incident neutron were $E_i = 8.11$ meV for 0.0 GPa, $E_i = 5.08$ meV for 0.3, and $E_i = 3.05$ meV for 1.4 GPa. Figure S1 (A and B) shows the INS spectra at 2.7 and 100 K under 0.3 GPa measured at HRC. At 2.7 K, flat excitations are observed at 0.9 and 1.5 meV in addition to the dispersive excitation below 1.0 meV. These flat excitations remain at 100 K, although the dispersive one disappears. The INS spectra at 0.9 and 100 K under 1.4 GPa are shown in fig. S1 (D and E). At 0.9 K, strong intensity is observed around $q = 0$ in addition to the dispersive excitation, and it remains at 100 K. We thus presume that the data measured at 100 K was the background from the pressure cell and cryostat. Then, the background was subtracted from the data at base temperatures for 0.3 and 1.4 GPa, as shown in fig. S1 (C and F).

In the CTAX experiment, the cell was installed into the $^4$He cryostat for 0.0, 0.3, 0.6, and 1.4 GPa and $^3$He cryostat for 0.8, 0.9, and 1.1 GPa. The energy of the final neutron was fixed to be $E_f = 3.5$ meV. A Horizontal-focusing analyzer was used to gain high intensity.
Table S2. Summary of parameters obtained from the refinement on the constant q scans

\[ q = (\mathbf{k}, 0, 0) \] at 1.4 GPa by Lorentzians convoluted by the experimental resolution functions.

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Data and materials availability: All data needed to evaluate the conclusions in the paper are present in the paper and/or the Supplementary Materials. Additional data related to this paper may be requested from the authors.

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Novel excitations near quantum criticality in geometrically frustrated antiferromagnet CsFeCl$_3$

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