Supporting information for article:

A routine for the determination of the microstructure of stacking faulted nickel cobalt aluminium hydroxide precursors for lithium nickel cobalt aluminium oxide battery materials

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S1. Additional tables and figures

| Original Cell | Transformed Cell |
|---------------|------------------|
| a = 3.029 Å   | a = 5.246 Å      |
| b = 3.029 Å   | b = 5.246 Å      |
| c = 4.647 Å no intercalation | c = 4.647 Å no intercalation |
| c = 7.533 Å intercalation | c = 7.533 Å intercalation |
| α = 90°       | α = 90°          |
| β = 90°       | β = 90°          |
| γ = 120°      | γ = 120°         |

* there cannot be two adjacent carbonates

**Figure S1** Illustration of the transformation of the unit cell of the brucite type NAC-precursor material in order to properly model the intercalation of carbonate ions and water molecules.
Figure S2  Comparison of the graphical results of the final Rietveld refinement of the NCA-precursor L002 by (a) using the faultless, brucite type structure, (b) at the global minimum (straight lines) of the one-dimensional grid search (Figure 7,a), the fit using the faultless structure model is presented in dashed lines, (c) at the global minimum (straight lines) of the two-dimensional grid search (Figure 7, b), the fit using the minimum of the one-dimensional parameter space is presented in dashed lines and (d) at the global minimum (straight lines) of the three-dimensional grid search (Figure 7, b), the fit using the minimum of the two-dimensional parameter space is presented in dashed lines.
Figure S3 3-dimensional parameter space including the probabilities of C19-, 3R- and interstratification-type faults, the black highlighted points of the grid represents microstructural models that yield almost identical Rwp values and therefore may represent the global minimum of the parameter hypersurface.

Figure S4 Evolution of the random distribution of the Rwp-factors for 100 recursively created and averaged superstructure of the NCA-precursor material while iteratively increasing the number of stacks per sequence (a-c) and while iteratively increasing the number of sequences (d-f). The ranges of the standard deviations (σ, 2σ and 3σ) are highlighted with backgrounds in different grey scale colours.
Figure S5  Evolution of the distribution of the Rwp-factors for 100 recursively created and averaged superstructure of the NCA-precursor material in dependence of the number of stacks per sequence (left) and the number of sequences (right). The average Rwp is indicated by a black square and the minimum and maximum Rwp is indicated by a horizontal black bar. The evolution of the time per iteration cycle in dependence of the number of stacks per sequence (left) and the number of sequences (right) is also presented. The average iteration time is indicated by a blue square and the variation of the iteration time is indicated by horizontal blue bars.

Figure S6  Illustration of a C19-type fault in the C6-type stacking that induces a subsequent intercalation.
Table S1  Applied transition probability matrices in the 3-dimensional final grid search (top) (Figure 7, c) and in the one-dimensional grid search for \( p_{\text{pref}} \) (bottom) (Figure 9, b). The stacking vectors are given in Figure 6. A, B, C, D, E, F refer to brucite-type layers, G refers to intercalation layers. Layers D, E and F had to be added as the c-component of the stacking vector cannot be varied within a row of the transition probability matrix in the TOPAS syntax.

| from/to  | A       | B       | C       | D       | E       | F       | G       |
|---------|---------|---------|---------|---------|---------|---------|---------|
|         | \( 1-p_{\text{car}}p_{x}p_{y} \) | \( p_{x} \) | \( p_{y} \) | \( p_{\text{car}} \) | \( p_{\text{car}}p_{x} \) | \( p_{\text{car}}p_{y} \) | 0       |
|         | \( p_{\text{car}} \) | S2      | S3      | \( 1-p_{\text{car}}p_{x}p_{y} \) | \( \text{S2} \) | \( \text{S3} \) |         |
|         | \( 1-p_{\text{car}}p_{x}p_{y} \) | \( p_{\text{car}} \) | S2      | S3      | \( p_{\text{car}} \) | \( p_{\text{car}}p_{x} \) | \( p_{\text{car}}p_{y} \) | 0       |
|         | \( p_{\text{car}} \) | S2      | S3      | \( 1-p_{\text{car}}p_{x}p_{y} \) | \( \text{S2} \) | \( \text{S3} \) |         |
| D       | 0       | 0       | 0       | 0       | 0       | 0       | 1, S4   |
| E       | 0       | 0       | 0       | 0       | 0       | 0       | 1, S4   |
| F       | 0       | 0       | 0       | 0       | 0       | 0       | 1, S4   |
| G       | 0       | 0       | \( 1-p_{\text{car}} \) | 0       | 0       | \( p_{\text{car}} \) | 0       |

| from/to  | A       | B       | C       | D       | E       | F       | G       |
|---------|---------|---------|---------|---------|---------|---------|---------|
|         | \( 1-p_{\text{car}}p_{x}p_{y} \) | \( p_{x} \) | \( p_{y} \) | \( p_{\text{car}}p_{x} \) | \( p_{\text{car}}p_{y} \) | \( p_{\text{car}}p_{x}p_{y} \) | \( 1-p_{\text{car}}p_{x}p_{y} \) | 0       |
|         | \( p_{\text{car}}p_{x} \) | S2      | S3      | \( 1-p_{\text{car}}p_{x}p_{y} \) | \( \text{S2} \) | \( \text{S3} \) |         |
|         | \( 1-p_{\text{car}}p_{x}p_{y} \) | \( p_{\text{car}}p_{x} \) | S2      | S3      | \( p_{\text{car}}p_{x}p_{y} \) | \( \text{S2} \) | \( \text{S3} \) |         |
| D       | 0       | 0       | 0       | 0       | 0       | 0       | 1, S4   |
| E       | 0       | 0       | 0       | 0       | 0       | 0       | 1, S4   |
| F       | 0       | 0       | 0       | 0       | 0       | 0       | 1, S4   |
| G       | 0       | 0       | \( 1-p_{\text{car}} \) | 0       | 0       | \( p_{\text{car}} \) | 0       |
Figure S7 Graphical results of the final Rietveld refinements of the NCA-precursor materials by averaging 100 supercells with 500 layers each and using transition probabilities given in Error! Reference source not found. The reflection positions of the ideal faultless brucite-type structure are given in each graph.
Figure S8  IR-spectra of the investigated NCA-precursor materials

S2. Demonstration of the grid search in TOPAS syntax

S2.1. One-dimensional grid-search

In order to perform a grid-search optimization in any parameter space, a TOPAS input-file has to be executed many times. This can be realized by the “num-runs” command (Table S2). The parameters, which should be optimized, are varied from one run to another by an incremental value. By including “##Run_Number##” into the syntax the run number is used as running index that increases from one run to the next one, as it is suggested for performing a series of simulations (Dinnebier et al., 2019). For a one dimensional grid search, the input file was executed 101 times, starting with run number 0 and ending with run number 100. The actual run number divided by 100 was used as parameter value for $P_x$. Hence, in the one dimensional grid search, $P_x$ was varied from 0.00 to 1.00 in 0.01 increments (Table S2). With a conventional PC or notebook, the one-dimensional grid search of the NCA-precursor samples takes approx. 40-50 minutes.
**Table S2**  Selected commands in TOPAS syntax that were used to perform a one-dimensional grid search in the parameter space of the transition probabilities.

| TOPAS-syntax          | Explanation                                                                 |
|-----------------------|-----------------------------------------------------------------------------|
| num_runs 101          | The input file is executed 101 times, i.e. 101 grid points are investigated.|
| seed                  | Before execution of the input file the random number generator creates a new set of random numbers |
| prm !px =(#Run_Number#/)/100; | The run number is used as a running index, starting at 0, from one run to the next one the parameter P\_x is increased by 0.01, which lead to P\_x = 1 in the last run. |
| out "grid-1D.txt" append Out(Get(r_wp),"t%11.5f") Out(px,"t%11.5f\n") | The Rwp value and the parameter value of P\_x are stored in a separate ASCII file, as the INP-file is not modified and not OUT file is created when “num_runs” is used |

**S2.2. Two-dimensional grid-search**

In a two dimensional grid search, two parameters: P\_x and P\_y are optimized simultaneously, i.e. a grid has to be created that contains all points from P\_x = 0.01 to P\_x = 1.00 and P\_y = 0.00 to P\_y = 1.00. If the parameters are varied in 0.01 increments, this grid will contain 10099 points (excluding P\_x = 1.00, P\_y = 0). In order to search all points, this grid is subdivided into 101 rows with each row containing 100 points (Table S3). Within a row P\_x is varied from 1.00 to 0.00 in 0.01 increments and P\_y is kept constant. When the grid search is completed in one row, i.e. P\_x = 0.00, another row is started, which means that P\_y is increased by 0.01 and P\_x switches back to 0.99. By using the “Round” command the grid is divided into 101 rows (“rrownumber”, Table S3) consisting of 100 points. In addition, the “Round” command provides integer value for the “rrownumber” running index that is increased by 1 after 100 runs. With a conventional PC or notebook, the two-dimensional grid search of the NCA-precursor samples took between (7 and 8) hours.
Table S3  Selected commands in TOPAS syntax that were used to perform a two-dimensional grid search in the parameter space of the transition probabilities.

| TOPAS-syntx | Explanation |
|-------------|-------------|
| num_runs 10098 | The input file is executed 10099 times; i.e. 10099 grid points are probed, starting at num_runs = 0. |
| prm rownumber = Round((##Run_Number##-49)/100); | The running index parameter “rownumber” is created that is in dependence on the Run_Number index. The round command provides an integer value for this parameter. The rownumber is increased by 1 after 100 runs. This provides a subdivision of the 10099 runs into 101 sets with 100 runs each. |
| prm px = ((rownumber*100+100)-(##Run_Number##+1))/100; | The transition probability P_x is varied from 1.00 to 0.01 in 0.01 increments during a set of 100 runs. At the beginning of a new set of 100 runs, P_x is set back to 1.00. |
| prm py = rownumber/100; | The transition probability P_y is varied from 0.00 to 1.00 in 0.01 increments. Within a set of 100 runs, P_y is kept constant. |
| out "grid-2D.txt" append Out(Get(r_wp),"t%11.5f") Out(px, "t%11.5f") Out(py, "t%11.5f\n") | The Rwp value and the parameter values of P_x and P_y are stored in a separate ASCII file |

S2.3. Three-dimensional grid-search

Extending a two-dimensional grid to a three-dimensional one in order to optimize both P_x, P_y and P_car requires both a further subdivision of the running index and an increase of the total number of runs. As a full three-dimensional grid search with all parameters varying from 0.00 to 0.99 in 0.01 increments contains 100x100x100 = 10000000 points and will take several weeks on a conventional PC or notebook, the grid search was limited to an excerpt of 0.10 ≤ P_x ≤ 0.24, 0.00 ≤ P_y ≤ 0.19, 0.04 ≤ P_car ≤ 0.09 in which the global minimum was expected based on the two-dimensional grid search and which only contains 1800 points. This grid search can be realized by combing several two-dimensional grid searches in the P_x-P_y parameter space (Table S3). Hence the three-dimensional grid is divided into two subdivisions:

1. rows that contain 20 points in which P_y is decreased from 0.19 to 0.00 in 0.01 increments and P_x and P_car are kept constant;

2. levels that consist of 15 rows, within a level P_x is increased from row to row from 0.10 to 0.24 in 0.01 increments and P_car is kept constant,
3. the entire parameter space is divided into six levels, $P_{\text{car}}$ is increased from level to level from 0.04 to 0.09 in 0.01 increments.

The TOPAS syntax for the three dimensional grid search is presented in Table S4. With a conventional PC or notebook, the two-dimensional grid search of the NCA-precursor samples took between (2 and 3) hours.
**Table S4** Selected commands in TOPAS syntax that were used to perform a three-dimensional grid search in the parameter space of the transition probabilities within a range of $0.10 \leq P_x \leq 0.24$, $0.00 \leq P_y \leq 0.19$, $0.04 \leq P_{\text{car}} \leq 0.09$.

| TOPAS-syntax                                                                 | Explanation                                                                                                                                 |
|-----------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------|
| num_runs 1799                                                               | The input file is executed 1800 times; i.e. 1800 grid points are probed, starting at num_runs = 0. |
| prm row = Round((##Run_Number##*5-49)/100);                                 | The running index parameter “row” is created that is always increased by 1.0 after the input file was executed for 20 times. This provides a subdivision of the 1800 runs into 91 sets with 20 runs each. |
| prm levels = Round((##Run_Number##/300)-0.49999);                           | For further subdivision of the running indices, an additional running index is introduced. The running index parameter “levels” is always increased by 1.0 after the input file was executed for 300 times. This provides a subdivision of the 1800 runs into 6 sets with 300 runs each. |
| prm rownumber = row-(levels*15);                                            | The running indices “row” providing a subdivision of sets of 20 runs and “levels” providing a subdivision of sets of 300 runs are linked by the parameter “rownumber” |
| prm !px = rownumber/100+0.1;                                                | The transition probability $P_x$ is varied from 0.10 to 0.24 in 0.01 increments. Within a set of 20 runs, $P_x$ is kept constant. |
| prm !py = (##Run_Number##/100)-(row*(20/100));                             | The transition probability $P_y$ is varied from 0.00 to 0.19 in 0.01 increments during a set of 20 runs. At the beginning of a new set of 20 runs, $P_y$ is set back to 0.00. |
| prm !pcar = 0.04 + levels/100;                                              | The transition probability $P_{\text{car}}$ is varied from 0.04 to 0.09 in 0.01 increments. Within a set of 300 runs, $P_{\text{car}}$ is kept constant. |
| out "grid-2D.txt" append Out(Get(r_wp),"t%11.5f") Out(px, "t%11.5f") Out(py, "t%11.5f") Out(pcar, "t%11.5f\n") | The Rwp value and the parameter values of $P_x$, $P_y$ and $P_{\text{car}}$ are stored in a separate ASCII file |