Inter-Turn Short-Circuit Fault Detection in Synchronous Reluctance Machines, Based on Current Analysis †

Kévin Henriques *, Khaled Laadjal * and Antonio J. Marques Cardoso *

CISE—Electromechatronic Systems Research Centre, University of Beira Interior, Calçada Fonte do Lameiro, P-6200-101 Covilhã, Portugal
* Correspondence: kevin.m.henriques@gmail.com (K.H.); laadjal.khaled1991@gmail.com (K.L.); ajmcardoso@ieee.org (A.J.M.C.)
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Abstract:Fault diagnosis in electrical drives can be very difficult, especially when the input data come from an operating electrical machine. The occurrence of inter-turn short-circuit (ITSC) faults is one of the most dangerous electrical machine failures, and if these are not detected at an early stage of development, they can result in serious consequences both in terms of repair cost and safety. In this context, an effective offline approach for diagnosing ITSC faults is proposed, which is based on the computation of a specific severity indicator. This does not require the determination of motor parameters and only involves the use of current sensors. Several tests were performed on a synchronous reluctance machine (SynRM), for various operating conditions (healthy and faulty). The obtained results confirm the effectiveness of the proposed technique for diagnosing ITSC faults, with high reliability, rapidity, and accuracy.

Keywords: inter-turn short-circuit fault; synchronous reluctance machine; current analysis; zero sequence of the current

1. Introduction

Nowadays, electrical machines are part of the day-to-day life of society, providing convenience and comfort in various domestic and industrial applications, and enabling technological development and growth. Thus, the need for them to remain in operation for prolonged periods of time has increased, and, consequently, motor malfunctions have started to appear; therefore, the need to diagnose malfunctions occurring in these machines has increased.

In the case of the motor under study, i.e., the synchronous reluctance motor (SynRM), the most common faults are found in the rotor circuit as inter-turn circuit faults. In this way, three groups of methods are presented in the literature for the detection of these faults: the analytical model-based method, the signal processing method and the knowledge-based method [1].

Analytical model-based methods need the models to be accurate, as in [2–4]. These methods are based on the comparison between a simulation model and an experimental model.

The signal processing method quantitatively analyzes the characteristics of a specific motor signal or conducts an observation of specific harmonics, as in [5,6]. The analysis of the current and voltage signals is obtained from the motor, or the application of the fast Fourier transform (FFT) is performed to obtain a spectrum that varies according to the operating conditions of the motor.

Finally, the knowledge-based approach uses artificial intelligence techniques for approaches through knowledge, as in [7–9].
This paper proposes a signal processing method that consists of acquiring the motor input currents and voltages. Then, the Fourier transform (FT) is applied offline to obtain the zero sequence of the current (ZSC) and after that we applied the FFT to obtain the spectrum of the current and voltage signals of the three phases. To demonstrate the efficiency of this technique, several experimental tests were carried out in open and closed loop control, with the aim of studying the behavior of the symmetrical components of the current in the presence of ITSC, under load variations.

2. Theoretical Context

In this chapter, the motor components are presented analytically for healthy and faulty operating conditions.

2.1. Healthy Motor

For a three-phase SynRM fed by a three-phase balanced voltage supply, which contains time harmonics (TH), the general equations for the three-phase currents are given by [10,11]:

\[
\begin{aligned}
    i_a(t) &= i_{TH}^\nu \cos(\nu \omega_s t) + i_{RSH}^{\nu\omega} \cos\left((\nu \omega_s + k \Omega_t \omega_r) t\right) \\
    i_b(t) &= i_{TH}^\nu \cos(\nu \omega_s t - 2\pi/3) + i_{RSH}^{\nu\omega} \cos\left((\nu \omega_s + k \Omega_t \omega_r) t - 2\pi/3\right) \\
    i_c(t) &= i_{TH}^\nu \cos(\nu \omega_s t - 4\pi/3) + i_{RSH}^{\nu\omega} \cos\left((\nu \omega_s + k \Omega_t \omega_r) t - 4\pi/3\right)
\end{aligned}
\]  

(1)

where \( \nu = 1, 3, 5, \ldots \) is the order of the TH, \( i_{TH}^\nu \) represents the amplitude of the TH, \( i_{RSH}^{\nu\omega} \) is the amplitude of the slot harmonic (RSH) as a function of \( \nu \), \( N_s \) is the number of slots of the rotor, \( \omega_r \) is the rotor speed, \( p \) is the number of pole pairs and \( k \) is an integer.

TH happens due to the power supply, while RSH is the result of the discrete distribution in the rotor slots. However, the SynRM, even in a healthy state, contains certain levels of both static and dynamic residual eccentricities. These are known as eccentricity fault harmonics (EFH) [10,11]. Thus, the frequencies can be expressed as follows:

\[ f_{EFH} = (\nu f_s + kf_r). \]  

(2)

In this way, the stator currents of a SynRM in a healthy state contain spectral components, which are related to the residual mixed eccentricity fault. Hence, it is possible to write:

\[
\begin{aligned}
    i_a(t) &= i_{TH}^\nu \cos(\nu \omega_s t) + i_{EFH}^{\nu\omega} \cos\left((\nu \omega_s + k \omega_r) t\right) + i_{RSH}^{\nu\omega} \cos\left((\nu \omega_s + k \Omega_t \omega_r) t\right) \\
    i_b(t) &= i_{TH}^\nu \cos(\nu \omega_s t - 2\pi/3) + i_{EFH}^{\nu\omega} \cos\left((\nu \omega_s + k \omega_r) t - 2\pi/3\right) + i_{RSH}^{\nu\omega} \cos\left((\nu \omega_s + k \Omega_t \omega_r) t - 2\pi/3\right) \\
    i_c(t) &= i_{TH}^\nu \cos(\nu \omega_s t - 4\pi/3) + i_{EFH}^{\nu\omega} \cos\left((\nu \omega_s + k \omega_r) t - 4\pi/3\right) + i_{RSH}^{\nu\omega} \cos\left((\nu \omega_s + k \Omega_t \omega_r) t - 4\pi/3\right)
\end{aligned}
\]  

(3)

\( i_{EFH}^{\nu\omega} \) is the amplitude of EFH as a function of \( \nu \), and \( f_r \) indicates the rotation frequency. Equation (3) shows that the stator currents for a healthy motor will have an infinite series of three types of harmonics: TH, EFH and RSH [10,11].

2.2. Faulty Motor (ITSC)

The existence of an ITSC creates, in the phase that it affects, a decrease in the resistance, followed by an increase in the current of the same phase [10,11].

The occurrence of an ITSC induces current harmonics in the stator with frequencies, which is given by:

\[ f_{ITSC} = \nu f_s + kf_r. \]  

(4)

in which \( f_r \) is the rotation frequency, \( \nu = 1, 3, 5, \ldots \) and \( k \) is an integer.

As can be noted, this equation is the same as Equation (2). Thus, it is possible to detect a clear ambiguity between the values of the mixed eccentricity and ITSC fault. So, in this context, the effect of an ITSC fault, in other words, is the same as a shorter winding; due to these shorter windings, the Magneto-Motive Force (MMF) produced is weaker. Furthermore, the current circulating in the short-circuited windings also produces an MMF.
that is opposite to the main MMF created by the phase windings. Consequently, the new MMF is the subtraction of the MMF induced by the short-circuited turns with the MMF generated by the stator in normal operation.

Therefore, the currents of the stator with ITSC fault can be given by:

\[
\begin{align*}
    i_a(t) &= i_{\text{TH}}^{\nu} |_{\text{SC}} \cos(\nu \omega_s t) + i_{\text{EFH}}^{\nu} |_{\text{SC}} \cos[(\nu \omega_s + k \omega_r) t] + i_{\text{RSH}}^{\nu} |_{\text{SC}} \cos[(\nu \omega_s + kN \omega_r) t - 2\pi/3] \\
    i_b(t) &= i_{\text{TH}}^{\nu} |_{\text{SC}} \cos(\nu \omega_s t - 2\pi/3) + i_{\text{EFH}}^{\nu} |_{\text{SC}} \cos[(\nu \omega_s + k \omega_r) t - 2\pi/3] + i_{\text{RSH}}^{\nu} |_{\text{SC}} \cos[(\nu \omega_s + kN \omega_r) t - 4\pi/3] \\
    i_c(t) &= i_{\text{TH}}^{\nu} |_{\text{SC}} \cos(\nu \omega_s t - 4\pi/3) + i_{\text{EFH}}^{\nu} |_{\text{SC}} \cos[(\nu \omega_s + k \omega_r) t - 4\pi/3] + i_{\text{RSH}}^{\nu} |_{\text{SC}} \cos[(\nu \omega_s + kN \omega_r) t - 4\pi/3]
\end{align*}
\]

(5)

where \(i_{\text{TH}}^{\nu} |_{\text{SC}}, i_{\text{EFH}}^{\nu} |_{\text{SC}} \) and \(i_{\text{RSH}}^{\nu} |_{\text{SC}} \) are the new amplitudes of TH, EFH and RSH, respectively, as a function of \(\nu\), after the presence of the short circuit.

3. Definition of the Indicator

3.1. Fast Fourier Transform (FFT)

This is a signal processing method; as discussed earlier, this method includes time, frequency, and time–frequency domain analysis approaches [12].

This represents a signal as a combination of multiple sinusoidal functions, and clearly shows the frequency distribution of a signal, representing the amplitude and frequency of the components of harmonics, which can be used to define machine malfunctions [13]. Monitoring through spectral analysis of signals consists of performing a simple \(x(t)\) transform of a continuous signal over time, thus allowing us to describe any signal in the frequency spectrum; the equation that allows this transformation is given by:

\[
x(f) = \int_{-\infty}^{+\infty} x(t) e^{-j2\pi ft} dt
\]

(6)

To perform the analysis of a signal over a finite period, a weighting window is needed to correct for the finite time effect. Therefore, the frequency accuracy depends on the sampling frequency \(f_s\) and the number of samples \(N\), as shown in:

\[
\Delta f = \frac{f_s}{N}
\]

(7)

The result of the previous equation is a frequency directly related to the modifications of the amplitudes of the harmonics, due to defects in the machine operation.

3.2. Fourier Transform (FT)

The indicator is calculated using FT. This technique consists of transforming an unbalanced system of polyphase vectors, in several balanced systems. Thus, for a three-phase system, an unbalanced set of voltages or currents can be transformed into two symmetrical three-phase systems with opposite phase sequences (negative and positive). Besides these two, there is still a third set of equal vectors, that is, zero phase sequence.

In this way, applying this transform to three-phase voltages \(V_a, V_b, V_c\) of a synchronous reluctance motor results in three symmetrical components: Positive \(V_+\), Inverse \(V_-\) and Zero \(V_0\). These components can be obtained with the following expression [14]:

\[
\begin{bmatrix}
    V_+ \\
    V_- \\
    V_0
\end{bmatrix} = \frac{1}{3} \begin{bmatrix}
    1 & a & a^2 \\
    1 & a^2 & a \\
    1 & 1 & 1
\end{bmatrix} \begin{bmatrix}
    V_a \\
    V_b \\
    V_c
\end{bmatrix}
\]

(8)

Then, the FT is applied to calculate the positive and negative sequences required. Figure 1 illustrates a diagram representing the implementation of the technique.
4. Experimental Study

The experimental bench used in the study consists of a SynRM with its windings modified by adding tappings. These make it possible to create ITSCs with different severities of fault. Together with the motor, there is a PMSM as a generator and an industrial inverter for supply. Figure 2 shows a general view of the bench and in Table 1 we present the parameters of the motor. The voltage and current measurements were made using Tektronix P5200A differential voltage probes, the Tektronix TCPA300 amplifier and Tektronix TCP312 current probes. The corresponding signals were acquired using a NI USB-6366 series data acquisition board with a 20 kHz sampling frequency. These steps were carried out continuously, which enabled the evolution of the indicators and the different magnitudes to be monitored in real time.

![Diagram of the implementation of the proposed technique](image)

**Figure 1.** Schematic of the implementation of the proposed technique.

![General view of the experimental test bench](image)

**Figure 2.** General view of the experimental test bench.

**Table 1.** SynRM parameters.

| Parameter                        | Value        |
|----------------------------------|--------------|
| Number of poles                  | 4            |
| Rated power                      | 2.2 kW       |
| Rated voltage                    | 400 V        |
| Rated current                    | 5.7 A        |
| Rated frequency                  | 50 Hz        |
| Rated speed                      | 1500 rpm     |
| Rated inductance of the axis d/q | 150/25 mH    |
| Stator resistance                | 1.71 Ω       |

4.1. Open-Loop Control

The experimental results performed with open-loop control are represented in Table 2, which shows the quantitative evaluation of the FFT of the indicators studied. These tests were performed for different scenarios of different severities and loads. As it is possible to observe, the third harmonic of current and indicator (ZSC) clearly demonstrates the evolution of the fault for different loads, as not being affected by load variation.
Table 2. Quantitative values for Ia and ZSC.

| Load | Healthy State | Faulty State | Variation (%) |
|------|---------------|--------------|---------------|
|      |               | 12 Turns     | 18 Turns      | 24 Turns      | 12 Turns | 18 Turns | 24 Turns |
| Ia   | 3Fs           | 0 Nm         | 0.01909      | 0.05215       | 0.07921  | 173%     | 315%     | 416%     |
|      |               | 10 Nm        | 0.02436      | 0.07129       | 0.1008   | 193%     | 314%     | 499%     |
| ZSC  | 3Fs           | 0 Nm         | 0.01327      | 0.03363       | 0.0512   | 153%     | 286%     | 380%     |
|      |               | 10 Nm        | 0.02087      | 0.04449       | 0.06338  | 113%     | 204%     | 346%     |

Therefore, Figure 3 shows a graph where it is possible to verify the evolution of the spectrum of the current and the indicator. Analyzing this, it is possible to detect that for both indicators, under different scenarios they show a similar evolution, increasing as the severity increases, proving the effectiveness of this technique to detect faults in open-loop control.

![Open-loop control graph](image)

Figure 3. Graph of the evolution of the fault.

4.2. Closed-Loop Control

In this case the tests were performed for a closed-loop control; in Table 3, a quantitative evolution of the FFT of the indicators is presented. Similar to before, these tests were carried out for different situations with varying loads and severities.

Table 3. Quantitative values for Ia and ZSC.

| Load | Healthy State | Faulty State | Variation (%) |
|------|---------------|--------------|---------------|
|      |               | 12 Turns     | 18 Turns      | 24 Turns      | 12 Turns | 18 Turns | 24 Turns |
| Ia   | 3Fs           | 0 Nm         | 0.0008708    | 0.001283      | 0.001351 | 47%      | 55%      | 350%     |
|      |               | 4 Nm         | 0.00506      | 0.00652       | 0.00727  | 29%      | 44%      | 50%      |
| ZSC  | 3Fs           | 0 Nm         | 0.0012       | 0.001258      | 0.001435 | 5%       | 20%      | 52%      |
|      |               | 4 Nm         | 0.004964     | 0.005263      | 0.005454 | 6%       | 10%      | 15%      |

In this way, Figure 4 shows a graph where it is possible to verify the evolution of the spectrum of the current and the indicator. By analyzing this, it is possible to see that for both indicators, in different situations, they show a similar evolution, increasing as the severity increases, proving the effectiveness of this technique to detect faults in closed-loop control.
5. Conclusions

A new technique of offline inter-turn short-circuit fault diagnosis was presented. Based only on the measurement of the three-phase input currents, the proposed strategy uses the FT to calculate the ZSC indicator; afterwards, with FFT the spectrum of the current in phase and the spectrum of ZSC were determined. This allows a fast and reliable detection of an incipient inter-turn short-circuit fault in the SynRM. An analytical study of the SynRM in healthy state and with inter-turn short circuit faults has been presented. The behavior of the proposed indicator has been studied experimentally. The obtained findings suggest that Ia and ZSC can be regarded as highly reliable indicators for ITSC fault diagnosis in SynRM applications with open-loop control and closed-loop control, and they also validate the accuracy and versatility of the proposed approach. In addition, future research will investigate its online application while considering the occurrence of ITSC faults in different phases, and the sudden variation of the load.

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