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Controlling a Team of Robots with a Single Input

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Abstract—We present a novel end-to-end solution for distributed multirobot coordination that translates multitouch gestures into low-level control inputs for teams of robots. Highlighting the need for a holistic solution to the problem of scalable human control of multirobot teams, we present a novel control algorithm with provable guarantees on the robots’ motion that lends itself well to input from modern tablet and smartphone interfaces. Concretely, we develop an iOS application in which the user is presented with a team of robots and a bounding box (prism). The user carefully translates and scales the prism in a virtual environment; these prism coordinates are wirelessly transferred to our server and then received as input to distributed onboard robot controllers.

Developing a novel distributed multirobot control policy which provides guarantees on convergence to a goal with distance bounded linearly in the number of robots, and avoids inter-robot collisions. This approach allows the human user to solve the cognitive tasks such as path planning, while leaving precise motion to the robots. Our system was tested in simulation and experiments, demonstrating its utility and effectiveness.

I. INTRODUCTION

Multirobot applications have been extensively explored in the literature, including monitoring [1], [2], manufacturing [3]–[5], and manipulation [6], [7]. Yet while these (and many other) applications have a potential impact well beyond the laboratory, most of the results can only be used by experts with programming and robotics experience, limiting their reach. Systems that can be used with graphical (or other) user interfaces are key to bridging the gap between researchers in the lab and the outside world. Most state of the art controllers allow a single user to provide input to only a single robot at a time. This does not scale and we seek to enable a single user to control many robots simultaneously with a single input.

Developing an end-to-end real-time solution for multirobot systems present numerous challenges. Two significant challenges are in designing an effective interface that allows a user to specify how to use the team of robots, and developing distributed coordination algorithms which guarantee that tasks will be completed. Both of these present significant challenges on their own, but developing a solution for both simultaneously is an extremely challenging task.

Developing a user interface for robots presents a valuable opportunity to bring the human in the loop. Humans and robots have many complementary strengths: while humans excel at high-level cognitive tasks, robots triumph when it comes to repetitive, computational ones. This notion of human-robot task delegation has inspired a significant amount of literature. In general, however, this literature does not address control, focusing instead on human-robot interfaces, such as determining useful tasks and how they might be specified [8], developing natural or intuitive gestures [9], creating image-based interfaces for nonexperts [10], evaluating the efficacy of interface technologies [11], or examining application-specific interaction issues [12].

In the multirobot domain, McCann et al. present a method by which multiple users can direct a team of robots [13], but this work does not address control and also only presents simulation results. Podevijn et al. present a method for controlling subgroups of swarms using arm gestures and a Microsoft Kinect [14]. However, since their swarm controllers do not guarantee convergence in environments with obstacles, long command sequences may result in order to guide stuck robots to their goals. Those works that do address control are typically for a single robot, such as using multitouch gestures to control an articulated robot [15].

There have been many works on synthesis of multirobot control policies from high-level specifications, e.g. using linear temporal logic [16] or structured english [17], but writing these specifications still requires a good deal of skill.

The contributions of this work are an end-to-end solution for navigating teams of robots from one location to another in complex environments. We present a solution that addresses distributed multirobot control in a way that enables the development of a simplified user-interface. We also present and demonstrate an example interface for the system. Our system relies on a human-in-the-loop making critical decisions about a multirobot team navigating an environment on a tablet-based multitouch display (using the Apple iPad). The iPad displays a virtual environment with four views (three orthographic and one isometric projection) and real-time robot positions for visual feedback (Fig. 1). The robots are enclosed by a bounding box (prism) which the user can translate and scale using multitouch gestures, maneuvering it to the desired location and avoiding obstacles. This gives the user the capability to decide which risks are worth taking, and how close to get to certain hazards. As the prism is manipulated, its coordinates are regularly recorded. The union of a subset of these recorded prisms defines the free space for the robots to navigate to their destination. Figure 2 provides a pictorial view of our control loop.

The benefits of this type user input are many. In applications when there are multiple risk factors involved it may be difficult to develop a proper navigation heuristic and a human may be able to make a quick and appropriate decision. Addi-
Section I. Formal Statement

Consider a team of $n$ homogeneous robots $V_R = \{r_i | i = 1, \ldots, n\}$ that must navigate to a destination set $\mathcal{D}$ in a shared, constrained, bounded environment. Each robot has the configuration $x_i \in \mathbb{R}^d$, $d \in \{2, 3\}$ representing its position in Cartesian space, with dynamics:

$$\dot{x}_i = u_i, \quad x_i \in X_i \subset \mathbb{R}^d, \quad i = 1, \ldots, n.$$  

In order to maintain safety, robots must maintain a minimum distance from each other, $\lambda_{\min} > 0$.

\textbf{Problem 2.1.} Consider a team of homogeneous robots $V_R$ with dynamics (1). For some initial state $x_0$ and destination $\mathcal{D}$, find a control policy which will drive the robots to within a bounded ball of $\mathcal{D}$ while avoiding collisions with the environment and maintaining a distance greater than $\lambda_{\min}$ between robots.

III. Preliminaries

We seek a solution to Problem 2.1 that can be synthesized automatically from high-level specifications. The controller must be usable by non-experts who may not have experience with code or robots. To that end, we have developed a solution that generates low-level controllers for individual robots from simple multitouch inputs on an iOS interface.

In this work, we assume

- a user is capable of navigating a rectangular prism via multitouch input in a constrained environment such that the final position of the prism encloses the set $\mathcal{D}$ without colliding with the environment;
- all agents are identical;
- the environment is static;
- robots initiate with at least $\lambda_{\min}$ distance between every pair of robots;
- each robot is capable of self-localizing;
- robots are capable of transmitting only their current pose to other robots within a radius $\delta > \lambda_{\min}$;
- robots are capable of globally receiving limited information from a server about the environment;
- the initial and goal points in the environment must be connected.

Note we make no assumption about the goal set other than being reachable, and that it can be enclosed by a final prism.

The controller is implemented in two parts: an iOS interface to receive and parse user input and display the current system state, and a Python-based server which receives user commands and interfaces with the robots via ROS [18].

A. Abstracting the Environment

The environment of the robots is determined by user inputs on the iOS interface. The interface shows real-time position of the robots in the environment, and an initial bounding box for the robots $P_0$. In 3-D, the robots’ bounding box is a rectangular prism; in 2-D, it is a rectangle. We assume obstacles do not exist within this initialized prism. We choose a rectangular prism since it is simply described by $2d$ halfspaces, and intersections are easy to compute. Other shapes can also be chosen, with changes to the virtual forces (Sec. IV). We henceforth refer to the rectangle or rectangular prism simply as a prism.

The user manipulates the prism on the screen (Fig. 1), dragging and scaling, so it navigates the space without contacting obstacles in the environment (while this requires the user to avoid obstacles, a physics engine could be used to detect and prevent collisions). Since the robot state is defined as a single point and does not capture the robot’s physical extent, on the interface the environment must be padded by the robots’ size to ensure robots do not collide with obstacles.

As the user manipulates the prism enclosing the robots on the screen, new coordinates are transmitted to a server,
where the union of a subset of those prisms is used as an abstraction of the environment. A detailed description of the iOS application is presented in Section VI-A. This abstraction of the environment defines the free space of the robots. In the current work, prisms must be axis-orthogonal (i.e., prism rotations are not allowed).

**Definition 3.1:** The free space of the robots is the finite union of rectangular prisms $F = \bigcup_{j=1}^{j} P_j$, which are a subset of the prisms generated by the multitouch interface that satisfy $\mu(P_j \cap P_{j+1}) \geq 0.5\mu(P_j)$, where $\mu(\cdot)$ is the Lebesgue measure of the set.

Figure 3 shows the free space of the robots generated from the iOS app in the experiment in Section VII-B.

Within each prism, a robot activates a different on-board controller which forces the robot to the centroid of the prism. Once within the next prism, the robot activates the controller for that prism, sequentially composing controllers until reaching the goal. For each robot, we call the prism in which it is located and for which control is active the current prism. The current prism is determined as the prism with the highest index in which the robot is located. This means that robots can skip over some prisms in the sequence, which is key to our proof of convergence. It is important to note that at any time step, the current prism across the team of robots need not be the same. In other words, the robots progress through the sequence at an individual pace.

**IV. Controller Synthesis**

The abstraction of the environment enables the use of a simplified control policy, while still providing guarantees of safety and convergence. Key to our approach is that a prism $P_j \in F$ must overlap the previous one $P_{j-1}$ by at least 50% of the volume (for $d = 3$) or area (for $d = 2$) of the previous prism $P_{j-1}$. This guarantees that the centroid of the current prism is inside the next prism in the sequence.

We use a “virtual force” to drive each robot to the centroid of its current prism. In the case of a single robot, once the robot has reached the current prism’s centroid it is inside the next prism in the sequence, and can switch to that prism’s virtual forces. Robots cannot move backwards in the sequence of prisms; the index of the next prism must be higher than that of the current prism. The case of multiple robots requires additional inter-robot forces to prevent collisions between robots.

Intuitively, we would like robots to be strongly repelled from the prism boundaries and into the safer, inner part of the prism, where they are eased toward the center. Specifically, at the prism boundary, infinite force must repel the robot, and the force must disappear to zero at the center.

There are many functions which would satisfy these requirements, including the negative gradient of a navigation function [19]. However, we choose a function that allows more control over the magnitude of the force within the prism without requiring hand-tuned parameters for each prism. Since we desire similar properties of the prism forces and interrobot forces (the force must be infinite at the minimum distance, and zero at the maximum distance), we use a generalized force function for both types of forces:

$$f(d) = \begin{cases} \infty, & d < 0 \\ \frac{\alpha}{d^\beta} - \gamma, & d \leq (\alpha/\gamma)^{1/\beta} \\ 0, & \text{otherwise} \end{cases}$$

Here, $d$ is a distance, and the parameters $\alpha, \beta, \gamma$ allow a user to tailor the function to their application, modulating the rate of change of the force while forcing it to disappear to zero over the desired length of influence $l = (\alpha/\gamma)^{1/\beta}$. Figure 4 shows how the magnitude of $f(d)$ changes as $\beta$ is varied for fixed length of influence $l = 1000mm$, $\alpha = 1000$, and $\gamma = \alpha/l^{1/\beta}$ (to achieve $f(d = 1000) = 0$).

**A. Prism Forces**

Each prism can be described as the intersection of $2d$ halfspaces $P_j = \{q \mid H_j q \leq K_j, q \in \mathbb{R}^d\}$ where $H_j = [H_{j,1}^T \quad H_{j,2}^T \quad \cdots \quad H_{j,2d}^T]^T$, with each row $\|H_{j,k}\|_2 = 1$.

The force on each robot $r_i$ from its current prism $P_j$ is the sum of the forces from each facet of the prism,

$$u_{i,j} = -\sum_{k=1}^{2d} f_i^p(d_{i,j,k}^p) H_{j,k}^T,$$

where:

$$d_{i,j,k}^p = K_{j,k} - H_{j,k} x_i$$

is the distance from robot $r_i$ to the $k^{th}$ facet of prism $P_j$, and $f_i^p(d_{i,j,k}^p) \equiv f(d_{i,j,k}^p)$ with parameters $\alpha$ and $\beta$ fixed across
all prisms, facets, and robots. We vary $\gamma$ between prisms and facets to fix the length of influence so that the force from each facet disappears to zero at the centroid (chose $\gamma$ such that the length of influence is half the length of the respective side of the prism). Figure 5 shows the vector field on a 2D prism in blue, with the next prism in the sequence in red.

**B. Interrobot Forces**

We use the same generalized force function to calculate interrobot forces. Let the distance between a pair of robots be $d_{i,m}^r = ||x_m - x_i||_2$. The minimum safe distance between robots is $d_{i,m}^r > \lambda_{\text{min}}$, where the robots are strongly repelled (with infinite force at $\lambda_{\text{min}}$). As mentioned in Sec. III, we assume that robots can transmit their current position to robots in a disk of radius $\delta$. To prevent unnecessary interaction at long distances, we allow robots’ positions to influence other robots at a maximum distance of $\lambda_{\text{max}} \leq \delta$. At $\lambda_{\text{max}}$, the interrobot force disappears to zero.

Let the $V_i \subseteq V_R$ be the set of robots within $\lambda_{\text{max}}$ distance of robot $r_i$. The interrobot force on $r_i$ is the sum

$$u_{i,R} = \frac{1}{|V_i|} \sum_{m \in V_i} f_i^r (d_{i,m}^r - \lambda_{\text{min}}) \frac{x_i - x_m}{d_{i,m}^r},$$

(4)

where $|V_i|$ is the cardinality of $V_i$, and $f_i^r (d_{i,m}^r) = f(d_{i,m}^r)$ with parameters $\alpha$, $\beta$ the same as for the prism forces, and $\gamma = \gamma^r$, fixed across all robots such that $(\alpha/\gamma^r)^{1/\beta} = \lambda_{\text{max}} - \lambda_{\text{min}}$. We divide by the number of robots to prevent unnecessary interaction at long distances, we allow robots’ positions to influence other robots at a maximum distance of $\lambda_{\text{max}} \leq \delta$. At $\lambda_{\text{max}}$, the interrobot force disappears to zero.

Let the $V_i \subseteq V_R$ be the set of robots within $\lambda_{\text{max}}$ distance of robot $r_i$. The interrobot force on $r_i$ is the sum

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(4)

where $|V_i|$ is the cardinality of $V_i$, and $f_i^r (d_{i,m}^r) = f(d_{i,m}^r)$ with parameters $\alpha$, $\beta$ the same as for the prism forces, and $\gamma = \gamma^r$, fixed across all robots such that $(\alpha/\gamma^r)^{1/\beta} = \lambda_{\text{max}} - \lambda_{\text{min}}$. We divide by the number of robots to prevent interrobot forces from overwhelming the prism force (we use this in Proposition 5.2). The input to each robot is the sum:

$$u_i = u_{i,j} + u_{i,R}.$$  

(5)

**C. Overcoming local minima by randomized subdivision**

Systems which rely on combining multiple potential functions can be subject to local minima. For example, Fig. 6 shows three scenarios where a perfect alignment of robot and prisms can prevent the progress of the robots.

The scenarios presented in Fig. 6(a-c) correspond to sets of measure zero, and even a slight misalignment of the robots will cause forces that will destabilize these unstable minima.

A simple distributed method can overcome these local minima. If a robot that is within the length of influence of another robot does not make progress toward the goal, and is not within $(n-1)\lambda_{\text{max}}$ of the goal, it can initiate its own subdividing sequence. Consider the robots in Fig. 6a. They can each independently subdivide prism 1 into a smaller subset, by choosing at random a facet to translate closer to itself by a random (but small) distance. For example, one robot might choose to reduce the facet to the right in Fig. 6b to the dashed line, while the other might choose to reduce that same facet to the dotted line. Then, each robot would apply the control input (3) for their individual new prism, changing the centroid it is attracted to, and displacing the balance between the forces. This sequence can continue until the robots are no longer in a local minimum, when they either revert back to the original prisms or proceed to a future one.

**V. Analysis**

In this section, we study the stability and convergence properties of the controller (5). We will show that all robots reach within $(n-1)\lambda_{\text{max}}$ geodesic distance of the goal.

Within the proofs, we call a robot that is not within $\lambda_{\text{max}}$ of any other robot a *singleton*. For a robot $r_i$, any robot within $\lambda_{\text{max}}$ belongs to its *group* (Note that a robot $r_m$ in the group of $r_i$ need not have the same group as $r_i$); we can also say these robots are connected as in a graph. For a robot $r_i$, any robot to which it is directly or indirectly connected is in its *extended group*. We measure progress toward the goal as transitioning to a future prism in the free space sequence of prisms.

First we show that no robot can escape the free space or collide with other robots.

**Proposition 5.1**: Singletons cannot escape the free space.

*Proof*: Assume WLOG that $x_i \in P_j$ and $P_j$ is the highest indexed prism for which this is true. There are two scenarios: (A) $r_i$ inside and (B) $r_i$ outside of the length of influence of the $k^{\text{th}}$ facet of $P_j$.

(A) If $r_i$ is within the length of influence of the $k^{\text{th}}$ facet, the control input (3) due to this facet pushes the robot away from this facet. Also, the control input due to the opposite facet has no affect, since $r_i$ is outside of the length of influence of the opposing facet. Therefore, $r_i$ will be driven away from the facet.
Proposition 5.2: Non-singletons cannot escape the free space or collide with other robots.

Proof: Assume that a robot has either (A) escaped the free space, or (B) gotten too close to another robot.

(A) If \( r_i \) has escaped the free space, this means the interrobot force has overcome the prism force of its last current prism \( P_j \), forcing \( r_i \) to exit through some facet of the prism, facet \( k \). Since the inward force due to the prism \( u_{i,j} \) on \( r_i \) is infinite at facet \( k \), this means there exists some infinite force to overcome \( u_{i,j} \). Since the interrobot forces are averaged among \( r_i \)'s group, the worst case is when a single robot \( r_m \) is pushing \( r_i \) directly into facet \( k \) with infinite force, thus \( ||x_m - x_i||_2 \leq \lambda_{\text{min}} \). But since \( r_i \) also imposes a force on \( r_m \), \( r_m \) must move away from \( r_i \), thus the interrobot force will decrease, and \( r_i \) will move inward from the boundary. Therefore, \( r_i \) cannot escape the free space.

(B) If \( r_i \) has gotten too close to another robot \( r_m \), this means the sum of the forces from the other robots in the group of \( r_i \) as well as the prism force have overcome the force from \( r_m \). \( r_i \) has gotten too close to \( r_m \) when \( ||x_i - x_m||_2 \leq \lambda_{\text{min}} \). Since we assume the robots initialize with distances between them greater than \( \lambda_{\text{min}} \), this means that at some time previous instant \( t \), \( ||x_i - x_m||_2 > \lambda_{\text{min}} \). Thus, at time \( t \), the force imposed on \( r_i \) from \( r_m \) is finite. Assume that the force driving \( r_i \) toward \( r_m \) due to other robots and the prism is infinite. At some \( t' > t \), \( r_i \) has moved closer to \( r_m \) and further away from the other robots and the prism boundary, such that the force from the other robots and the prism boundary is now finite. Since this force pushing \( r_i \) toward \( r_m \) is finite, it cannot overcome the infinite force at \( ||x_i - x_m||_2 = \lambda_{\text{min}} \), therefore this cannot occur.

Since we have shown that robots cannot escape the free space and cannot come within \( \lambda_{\text{min}} \) of other robots, we now show that all robots make progress toward the goal.

Proposition 5.3: Singletons make progress toward \( D \).

Proof: Assume WLOG that the singleton \( r_i \) is in \( P_j \) and the next prism in the free space sequence is \( P_{j+1} \). Also assume that \( x_i \notin P_{j+1} \). \( u_{i,j} \) drives \( x_i \) to the centroid of \( P_j \). Since \( P_{j+1} \) overlaps at least 50% of \( P_j \), the centroid of \( P_j \) is inside \( P_{j+1} \), and the robot progresses to \( P_{j+1} \). This is true for any index \( i \) in the set \( P \), therefore the singleton will always make progress toward the goal.

Now we show that in a group of robots, at least one makes progress, and by recursion, all make progress.

Proposition 5.4: In a group of non-singleton robots, at least one robot makes progress toward \( D \).

Proof: In an extended group of non-singletons, where none of the robots are in the last prism, there are two cases.

(A) If the robots are not stuck in a local minimum, at least one robot is moving until (1) it proceeds to a future prism (since by construction robots cannot move backwards in the sequence), in which case one robot has made progress, or (2) eventually the group comes to equilibrium at a local minimum, in which case (B) applies.

(B) If the robots are stuck in a local minimum, the robots will initiate the random modification of their current prisms presented in Sec. IV-C. Since the adjusted facet and the adjustment size is chosen at random, eventually the robots will end up with unequal prisms. This will change the centroid that each robot is moving towards, disrupting the balance of forces. Eventually, due to the random nature of the modification, at least one robot will break out of the local minimum and progress to a future prism.

While Proposition 5.4 applies for a fixed group, if the group changes (by robots joining or exiting) we can apply the same results to the new group.

Corollary 5.5: All robots progress toward the last prism.

Proof: Follows by recursion on Proposition 5.4.

Theorem 5.6: Consider the system (1) in the space \( \mathcal{F} \), with control input (5). Every robot reaches within \((n-1)\lambda_{\text{max}}\) geodesic distance of the centroid of the last prism.

Proof: Assume WLOG that \( r_1 \) has reached equilibrium and is not within \((n-1)\lambda_{\text{max}}\) geodesic distance of the last prism. By Proposition 5.4, local minima cannot appear in a group where none of the robots are in the last prism. Therefore, at least one robot, which we call WLOG \( r_2 \), in the extended group of \( r_1 \) is in the last prism. However, since there are only \( n \) robots, and the maximum length between each pair of robots is \( \lambda_{\text{max}} \), the maximum geodesic distance between \( r_2 \) and the robot farthest away must be \((n-1)\lambda_{\text{max}}\).

This contradicts our assumption, and therefore \( r_1 \) must be within \((n-1)\lambda_{\text{max}}\) geodesic distance of the last prism.

Theorem 5.7: The control policy (5) solves Problem 2.1.

Proof: By Theorem 5.6, all robots reach within \( n\lambda_{\text{max}} \) geodesic distance of the last prism. By our assumptions in Sec. III, the goal \( D \) is within the last prism. Therefore the maximum distance between any robot and the goal \( D \) is the sum \((n-1)\lambda_{\text{max}} + ||L||_2\), where \( L \) is the length of the diagonal of the last prism.

VI. IMPLEMENTATION

As mentioned previously, the controller is implemented in two parts: an iOS interface and a Python server. Communication between the two components is handled via TCP websockets. The iOS interface is used solely for input and rendering; computation is done on the server side.

While we use a central server to handle controller input, control is distributed and does not require a centralized server. The server functionality could be moved to the input device or the robots and operated in a distributed fashion.

A. iOS Application

The iOS application presents the user with a virtual environment in which a prism can be translated and scaled to construct the robots’ free space. Although we use iOS, no iOS-specific features were used and any multitouch platform...
The server is in charge of two main tasks. First, it accepts
the current vertices of the prism from the iOS application and
decides whether to broadcast it over ROS topics. Second, it
periodically transmits the current locations of the agents to
the iOS application for display. We used Twisted [22] to
implement our event-based server.

The first task of the server is implemented in Algorithm 1. The server begins with knowledge of the last broadcast
prism, which we call the old prism. It then uses the appro-
appropriate method to compute the overlap between the old
prism and the latest received prism. If the overlap is greater
than some user-specified threshold \( \geq 50\% \) (80\% was used in
our experiments) but smaller than any other prism received
so far, that is retained in memory as the “best” prism. Once
the computed overlap dips below the set threshold or the old
prism’s centroid is not located in the new prism the server
broadcasts the best prism and repeats the process.

For axis-aligned rectangular prisms, calculating intersec-
tions is trivial. However, to allow for future extensions with
rotated prisms, we use QHULL [23] to compute intersections
and ensure the centroid of the original prism is inside the next
one. Since data is transmitted wirelessly, we assume the rate
of touch input, thus the rate of generation of prisms, is high
enough that the algorithm is robust to dropped packets.

Since the last prism may not satisfy the overlap threshold,
the server automatically broadcasts if no prisms have been
broadcast within a certain time (3 seconds in our implemen-
tation) to ensure the final prism generated is broadcast.

### VIII. Simulations and Experiments

We have tested our controller in various simulations and
experiments. Here we present two interesting and successful
results, which are also shown in the supplementary video.
Experiments use the Ascending Technology Hummingbird
quadrotors (we also base our simulations on these). The
controller runs in real time in a distributed way on a single
computer (each robot has their own thread and clock). For
both the simulated and physical systems, we used the inputs
generated by (5) to create waypoints for the system. Since
this is a discrete implementation of a continuous controller
with possibly infinite inputs, we saturate the maximum
control input to each robot, and ensure that the waypoint
being assigned to any robot is within its current prism.

It is important to note that everything occurs in real time.
Robots have no prior information about the environment, and
receive prism vertices only as the user manipulates the prism
on the app. Robots receive only the current location of other
robots within communication range, not knowing what other
robots’ or their own trajectory will be.

Waypoints update at 10Hz, but actual position is used
every 4 time steps, with each robot estimating their progress
and updating their waypoint in between. This accounts for
some of the jitter in the robots’ positioning as can be seen
in the plots and on the supplemental video.

In our experiments and simulations, we require a prism
overlap of 80\%. In general, the lower the percentage, the
smoother the trajectory, but choosing too low of a percentage
slows progress, as robots move more slowly near the centroid
of their current prism. Choosing too high creates very similar
cubes in the free space, thus the robots switch controllers
very often, resulting in increased jitter.

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**Algorithm 1:** Chooses subset of prisms for the free space

ReceivePrism(curr_corners, curr_scale):

1. Constant threshold\_{ratio}
2. Initialize(best\_prism, best\_volume, best\_ratio =
   1.0, old\_corners, old\_scale)
3. if Prism is scaling then
   new\_volume ←
   curr\_scale[x] * curr\_scale[y] * curr\_scale[z]
4. if Prism is shrinking then
   ratio ← new\_volume / old\_volume
5. else Prism must be growing
   ratio ← old\_volume / new\_volume
   end
6. else Prism is translating
   overlap ← Intersect(curr\_corners, old\_corners)
6. end
7. if ratio > threshold\_{ratio} then
   if ratio < best\_ratio then
      best\_corners ← curr\_corners
      best\_ratio ← ratio
      best\_volume ← new\_volume
   end
8. else Overlap is below allowed threshold
   old\_corners ← best\_corners
   best\_ratio ← 1.0
   old\_volume ← best\_volume
9. Broadcast(best\_corners) // Broadcast
   prism position to ROS topic
10. end

---

could be used instead. The display features four views: three
orthographic and one isometric view (see Fig. 1).

The views feature static opaque world objects such as
floors and obstacles (loaded from an XML file) and the
translucent prism (with a trail of previous prisms). The initial
dimensions of the prism are selected to bound all of the
agents and allow them to rise from the ground to initialize.
The prism can be translated with a touch and drag gesture or
scaled with a “pinch-to-zoom” gesture within any orthogonal
view (see Fig. 1). As the prism is manipulated, its vertices
are sent to the Python server. If desired, a physics engine
such as Open Dynamics Engine [20] could be employed to
perform collision checking, ensuring that the prism is not
allowed to intersect with any static world objects.

Although we used an iPad (running iOS version 6.1.2) for
our experiments, the iOS implementation can feasibly run on
any iOS device with version 4.2 or higher (to support web
sockets). iSGL3D [21] was used for graphics rendering.

**B. Server implementation**

The server periodically transmits the current locations of the agents to

the current vertices of the prism from the iOS application and

decides whether to broadcast it over ROS topics. Second, it

periodically transmits the current locations of the agents to
Fig. 7: Sequential frames in a five quadrotor simulation. Robots initiate on the left side, and must navigate to the right.

Fig. 8: Results from a 5-robot simulation. The environment is grey, with $+y$ wall removed for clarity. (top) Prisms composing the free space in yellow in a side view. (middle) Isometric view of trajectories. (bottom) Top view of trajectories.

Fig. 9: Distance between robot pairs in 5-robot simulation. $\lambda_{\min} = 600\text{mm}$ is maintained.

A. Simulations

We have tested the system in simulations with up to 5 robots in four different environments. Figure 7 shows the initial, a middle, and final frame of a representative simulation with $n = 5$ robots in a complex environment as it appears in the bottom left view of the iOS interface. The goal is to maneuver robots through the trench from the left to the right side. In the left frame, the system initiates with a prism enclosing all robots (robots occluded by obstacles are shown with a yellow dot). In the middle frame the user manipulates the prism to navigate it through the environment; the prism need not be large enough to accommodate all robots. In the right frame, all the robots have made it into the final prism.

B. Experiments

We ran experiments with up to 3 quadrotors in five environments. Here we show an experiment with $n = 3$ quadrotors in an environment with an obstacle. The environment and app-generated free space is shown in Fig. 3. In this experiment, three quadrotors rise over the obstacle via translating the prism, change configurations when the prism is scaled, then land on the opposite side of the obstacle via another translation. We use a 12-camera VICON motion capture system [24] for localization, and a linear-quadratic regulator (LQR) takes waypoints and generates low-level commands which are sent to each robot via XBee-Pro.

Isometric and top views of the experiment are shown in Fig. 10. The robots initiate at the colored circles and the reach equilibrium at the triangle marker. The distance between the robots is shown in the panel on the right. One notable result is how much the robots outperform the convergence guarantee. Although we guarantee robots’ reach within a distance $(n - 1)\lambda_{\max}$ of the final prism, which would be 1700 mm, all robots reach within 200mm of the final prism (red: 40mm, green: inside, blue: 188mm). This is representative of all of our simulations and experiments; the robots get much closer to the final prism than the guarantee. The distance between the farthest robot and the last prism is heavily dependent on the size of the prisms. The smaller the prisms, the less room for robots to fill in the final prism.

One notable result from this run that may at first appear to be cause for concern: one pair of robots break the minimum distance constraint $\lambda_{\min} = 850\text{mm}$ (the blue and red robots in the trajectory plots; the minimum distance between them is 638mm). This is likely a consequence of a number of factors. First, we are implementing a continuous controller (5) on a discrete system, which, to account for noise, updates at a forcibly slow rate. Second and more significantly, the air flow around the quadrotors creates an unmodelled irregular noise that can greatly affect the performance of both robots (850mm is extremely close, as the robots themselves have a radius of 270mm leaving approximately 310mm between the rotors of two robots). Our system does not model the on-board LQR controller, and properly calibrating the LQR gains to account for the expected noise in the system would prevent the robots from getting too close. How to set these gains is outside the scope of this paper, although we note that this is a one-time pre-processing step for a given cluster of robots and set of expected conditions (though such tuning might not be required for all vehicles). It is worth noting that the robots recover gracefully from this failure, demonstrating the robustness of our system.

VIII. Discussion

We have presented a novel distributed control policy for multirotor navigation designed specifically to be synthesized using only inputs from a straightforward, simple multitouch
interface created for non-experts. We provide an end-to-end solution for navigation of a team of robots from one location to another in a constrained environment with obstacles that provides guarantees on convergence and safety with simple multitouch gestures as input. The interface allows the user to decide a general path for the robots, allowing the user to evaluate the quality and risk of different available paths rather than creating a complex controller. This gives the user the ability to determine which risks should be taken and how close robots should get to certain obstacles. Such end-to-end solutions lower the barrier of entry to multirobot systems, enabling even those who have never programmed or used a robot to operate teams of robots.

Although our current system is robust, it does have limitations. Using a single prism to enclose the robots at initialization may not be feasible in some environments, where obstacles may exist between the robots. Merging multiple initial prisms, while resulting in a more complex interface to indicate merging, is a straightforward extension of this work. Splitting into multiple sets of prisms, however, is a more complex problem we plan to investigate. We also plan to incorporate rotations of the prism, which would allow the robots to more easily navigate more complex environments, such as those with ramps.

We have produced a simple interface to demonstrate that a controller that guarantees safety and convergence can be determined using very high-level inputs. The user experience, however, is not fully addressed in this work. Various design choices, e.g., particular gestures and views, remain unevaluated at this time. Designing a truly intuitive user interface requires coordinating with experts in the field, as well as extensive user studies. This is a subject of ongoing work.

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