Long-lifetime Polariton BEC in a Microcavity with an Embedded Quantum Well and Graphene

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We study the propagation of a Bose-Einstein condensate (BEC) of long-lifetime exciton polaritons in a high-quality microcavity with an embedded semiconductor quantum well or a graphene layer using the Gross-Pitaevskii equation. It is shown that in these heterostructures the BEC of the long-lifetime polaritons can propagate over the distance up to 0.5 mm. The obtained results are consistent with the recent experimental observations for GaAs/AlGaAs microcavity. It is demonstrated that the BEC density in a polariton trace in a microcavity with embedded graphene at large distances from the excitation spot is higher for the microcavity with higher dielectric constant. It is also predicted that the propagation of a polariton BEC in a microcavity with graphene is dynamically tunable by changing the gap energy, that makes it potentially useful for applications in integrated optical circuits.

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I. INTRODUCTION

Polaritons are the quantum superposition of photons and excitons in semiconductors or graphene \[1,3\]. In the past years, formation and spreading of the polariton Bose-Einstein condensate (BEC) in quasi-two-dimensional structures attract attention of experimentalists and theoreticians from the point of view of fundamental physics at nanoscales and due to potential applications of polaritons in integrated circuits for optical and quantum computing \[4,5\]. Because the effective mass of the polaritons is much smaller than the atomic masses, the BEC transition temperature is much higher than that for atomic BECs \[6\]. Another important features of the polariton BEC dynamics is that it is essentially non-equilibrium due to the finite polariton lifetime. The polariton decay is mainly caused by the leakage of photons from an optical microcavity and usually the polariton lifetime is of the order of a few picoseconds, depending on the quality Q-factor of the microcavity \[3\]. It was established that the polariton BEC can move in a planar microcavity in response of the external force or field \[8,9\]. However, in “traditional” experiments the characteristic length over which the BEC can spread in the microcavity is limited due to relatively short lifetime of the polaritons \[9\].

The signatures of the polariton BEC were first observed in GaAs-based microcavity \[10,12\] and then in CdTe-based \[16\] and GaN-based microcavities \[17\]. There are two advantages for observation of a polariton BEC in such heterostructures over a conventional exciton BEC \[18\]. First, polaritons have an effective mass, which is \(\sim 10^{-4}\) times lower than the exciton mass, that results in much higher critical temperature of the BEC transition for polaritons than that for the exciton BEC at the same particle density \[1,19,20\]. Second, the polariton BEC is less sensitive, compared to the exciton BEC, to the disorder caused by unavoidable crystal defects and impurities. It is worth noting that the presence of the defects results in the exciton localization in a fluctuating potential in a sample and can destroy an exciton BEC \[21,22\].

It was found \[10,12,13,10,25,29\] that for optimal conditions of the polariton BEC formation the quality Q-factor of the optical microcavity should be enough high. The increase of the microcavity Q-factor leads to the increase of the polariton densities in the microcavity and, also, to longer polariton lifetime thus presenting more favorable conditions for the BEC observations. Also, enough strong exciton-photon coupling (Rabi splitting) is needed thus, requiring large quantum well (QW) exciton oscillator strength. Enough large polariton-polariton interaction scattering cross-section is also an important factor, which provides efficient thermalization in the polariton system and hence short enough relaxation time for the transition of the system to a BEC (see Ref. \[19\] for the discussion). Rapid expansion of a spatial coherence and the polariton BEC formation dynamics in a GaAs-based microcavity has been recently observed in Ref. \[30\].

In the present Article we consider the dynamics of polaritons formed by the cavity photons and the excitons in GaAs a quantum well and graphene embedded in a microcavity. Our studies are motivated by experiments \[8\] and \[31\] where the directional propagation of exciton polaritons have been observed in the presence of an external force. In particular, in Ref. \[31\] the possibility of synthesis of a semiconductor microcavity with the Q-factor exceeding \(10^5\) has been demonstrated for the first time. That allowed one to observe the polaritons with extremely long lifetime \(\sim 100\) ps, that is \(\sim 30\times\) longer than that in the traditional experiments \[3\]. It was found \[31\] that the long-lifetime polaritons in a planar microcavity could propagate over a macroscopic scale of a fraction of millimeter order. It was supposed in Ref. \[31\] that a BEC coherent flow formed at high enough densities of the long-lifetime polaritons have promoted their long-distance propagation. In this Article, we demonstrate that the polariton dynamics observed in
Ref. 31 is consistent with that predicted from the Gross-Pitaevskii equation for a polariton BEC. Specifically, we show that under the action of an external force, a long-lifetime polariton BEC can propagate over the distance ~ 0.5 mm from the excitation spot. It is demonstrated that the polariton-exciton interactions can also significantly change the spatial distribution of the polaritons in the BEC. Based on the obtained results, we propose an observation of long-lifetime polariton BEC formed in a graphene layer embedded into a high-Q microcavity. It is shown that for graphene there is an additional controlling parameter – the energy gap in the electron and hole excitation spectra – that allows one to govern the polariton BEC propagation. The possibility to dynamically adjust the properties of the polariton BEC by changing the gap, for example through application of the electric field, makes a microcavity with embedded graphene a promising candidate for the use in adaptive optical circuits.

Our article is organized in the following way. In Sec. II the dynamics of a Bose-Einstein condensate of long-lifetime exciton polaritons in a microcavity with an embedded semiconductor quantum well or a graphene layer is considered based on the Gross-Pitaevskii equation. The details of the numerical simulations are presented in Sec. III. Sec. IV presents the results of the simulations of the polariton BEC propagation in a microcavity with an embedded quantum well and an embedded graphene layer. Here, the effect of the polariton lifetime on the BEC dynamics is discussed and the comparison of the BEC propagation in a microcavity with an embedded quantum well and graphene is presented. Finally, the conclusions follow in Sec V.

II. DYNAMICS OF AN EXCITON-POLARITON BEC IN A MICROCAVITY

At temperature much lower than the BEC transition temperature the dynamics of the exciton polariton BEC is described by the Gross-Pitaevskii equation

\[ i\hbar \frac{\partial \Psi(r, t)}{\partial t} = -\frac{\hbar^2}{2m} \Delta \Psi(r, t) + U(r)\Psi(r, t) + g\Psi(r, t)|\Psi(r, t)|^2 - i\hbar\gamma \Psi(r, t) + i\hbar G(r). \]  

In Eq. 1 \( \Psi(r, t) \) is the condensate wave function which depends on the coordinates \( r = (x, y) \) in the plane of the microcavity and time \( t \), \( m \) is the polariton mass, \( g \) is the effective interaction strength proportional to the polariton-polariton scattering amplitude, \( \gamma = 1/2\tau \) is the decay rate, \( \tau \) is the polariton lifetime, and \( G(r) \) is the source term. The term \( U(r) \) is defined as \( U(r) = U_{\text{ex-pol}}(r) + U_{\text{ext}}(r) \) describes the repulsive interaction \( U_{\text{ex-pol}}(r) \) of the polaritons with those excitons in a quantum well, which are not coupled with the microcavity photons, and the potential energy due to the external force, \( U_{\text{ext}}(r) \). Importance of the interactions of polaritons with the exciton cloud has been recently discussed in Ref. 32. The corresponding interaction energy is

\[ U_{\text{ex-pol}}(r) = X_0 g_{\text{ex-ex}} n_{\text{ex}}(r), \]  

where \( X_0 \equiv X_{k=0} \) is the Hopfield coefficient for the exciton component in the polariton wave function taken at the wave vector \( k = 0 \), \( g_{\text{ex-ex}} \) is the exciton-exciton repulsive interaction constant and \( n_{\text{ex}}(r) \) is the exciton density in the cloud. The Hopfield coefficient for arbitrary wave-vector \( k \) is

\[ X_k = \frac{1}{1 + \left( \frac{\hbar \Omega_R}{k_{\text{LP}} g_{\text{ex-pol}}(r)} \right)^2}, \]  

where \( \Omega_R \) is the Rabi splitting,

\[ E_{\text{LP}}(k) = \frac{E_C(k) + E_X(k)}{2} - \frac{1}{2} \sqrt{(E_C(k) - E_X(k))^2 + 4(h\Omega_R)^2} \]  

is the energy of the lower polariton branch, \( E_X(k) \) is the exciton energy and \( E_C(k) \) is the cavity photon energy as functions of \( k \). Because the polaritons in the BEC are condensed into the state with small wave-vectors \( k \), the Hopfield coefficient in Eq. 2 is taken at \( k = 0 \). We approximate the exciton density in the cloud via a Gaussian profile

\[ n_{\text{ex}}(r) = n_0 \exp(-|r - r_0|^2/a^2) \]  

where \( n_0 \) is the density at the center of the cloud and \( a \) is the characteristic size of the cloud. The Gaussian profile gives the required bell-like dependence for the exciton density in the excitation area \( |r - r_0| \sim a \). Also it captures the sharp drop of the exciton density at large distances \( |r - r_0| \gg a \). Thus, the polariton-exciton interaction is represented as

\[ U_{\text{ex-pol}}(r) = U_0 \exp(-|r - r_0|^2/a^2), \]  

where \( U_0 = X_0^2 g_{\text{ex-ex}} n_0 \). To study the effects of the polariton-exciton cloud interaction, we vary the interaction strength \( U_0 \) as described below.

It has been demonstrated in recent experiments 8 31 that the microcavity polaritons can be accelerated by an external force due to the spatial gradient of thickness of the microcavity. In this approach, the average force acting upon a polariton wave packet at the point \( r \) is \( F(r) = -\nabla E_C(r) \), where \( E_C(r) \) is energy of the polariton band taken at the in-plane vector of the polariton \( k = 0 \). In particular, in experiments 8 31 the microcavity width, and hence the energy \( E_C(r) \), has been a linear function a spatial coordinate (the wedge-shape geometry of the microcavity) that resulted in a constant \( U_{\text{pol}}(r) \equiv U_0 \) in the excitation area \( |r - r_0| \sim a \) and also captures the sharp drop of the exciton density at large distances \( |r - r_0| \gg a \). To describe the effect of the force, we set the corresponding potential energy as

\[ U_{\text{ext}}(r) = -F_0 x. \]  

To explore the polariton BEC dynamics in a macroscopically large sample we consider the case where the source of polaritons, \( G(r) \), is localized in space 29. Within the used approximation, the source term is represented as \( G(r) = G_0 \exp(-|r - r_0|^2/a^2) \) with the same characteristic size \( a \) as for the exciton cloud size.
The exciton effective mass in graphene. However, its exact value where $\delta = 0.1$ eV to 0.5 eV that are the representative values for graphene. The polariton lifetime is mainly defined by the leakage of the photons through the mirrors and only weakly depends on the exciton lifetime $\tau$. Therefore, we use the same polariton lifetime $\tau = 100$ ps for graphene and for a semiconductor quantum well.

### III. NUMERICAL SIMULATIONS

To study the polariton BEC dynamics, we numerically integrated Eq. (11). At the initial moment $t = 0$ we set $\Psi(r, 0) = 0$. As is demonstrated in Sec. LV below, the long-lifetime polaritons accelerated by the external force can propagate over distances up to $l_{\text{max}} \approx 0.5$ mm from the excitation spot. The characteristic wavelength of the polariton wave packet at the distance $l \approx l_{\text{max}}$ can be estimated quasiclassically as $\lambda_{\text{min}} \approx 2\pi/\sqrt{2n_F l_{\text{max}} + U_0}$ that gives $\lambda_{\text{min}} \approx 9.5 \times 10^{-7}$ m for $F_0 = 13$ meV/mm and $U_0 = 10$ meV. At shorter distances $l < l_{\text{max}}$ one has $\lambda > \lambda_{\text{min}}$. To resolve the oscillations of the polariton wavefunction with the wavelengths $\lambda \geq \lambda_{\text{min}}$, we choose the numerical grid spacing $\Delta x \approx 1.5 \times 10^{-7}$ m. The dimensions of the numerical box are $L_x \times L_y = 6000 \times 3000 \times (\Delta x)^2$. The long side of the numerical box is arranged parallel to the direction of the constant force $F_0$. We use the periodical boundary conditions at the numerical box boundaries. The unit of time is equal to $\Delta t = 2\pi/\Delta x^2$/h = $3.9 \times 10^{-14}$ s. We numerically integrated Eq. (11) over time with the 4th order Runge-Kutta scheme at the time step $h = 10^{-2} \Delta t$. An explicit 4th order accuracy method has been used to represent the Laplacian operator in Eq. (11). We took advantage of the graphical processing unit CUDA programming that allowed us to achieve ~ 20× increase of the performance with respect to the shared-memory parallel version of the code. This allowed us to perform the simulations for this macroscopic system within practically realizable time intervals. The overall computation time for a single run was ~ 10 hours on NVIDIA Tesla S2050 card.
IV. PROPAGATION OF A BEC OF LONG-LIFETIME POLARITONS IN A MICROCAVITY

A. Polariton BEC in a microcavity with an embedded quantum well

In this Section we focus on the propagation of a BEC of long-lifetime polaritons in a microcavity with an embedded semiconductor QW. Fig. 1 shows the time dependence of the total number of polaritons $N_p(t) = \int |\Psi(r, t)|^2 \, dr$ after the source it turned on. It follows from Fig. 1 that after the system approaches a steady state at $t \sim 6 \times 10^5 \Delta t \approx 230$ ps, for the pumping rate $G_0 = 0.1 \Delta x^{-1} \Delta t^{-1}$ the total number of polaritons is $N_p \sim 5.3 \times 10^4$ that is a representative value for experiments with exciton polaritons in a semiconductor microcavity [31]. Below we used this pumping rate in our simulations.

Propagation of long-lifetime polariton BEC in the quantum well plane is shown in Fig. 2. The center of the excitation spot is positioned at $r_0 = (x_0, y_0)$ where $x_0 = y_0 = 1500 \Delta x$. The evolution of the long-lifetime polariton BEC distribution with increasing of the force $F_0$ is given in Fig. 2a-c. Fig. 2a shows that in the absence of the force the polariton spot is symmetric in the $(x, y)$ plane and has a characteristic size of $\approx 500 \Delta x = 75 \mu$m that is, $\approx 7.5 \lambda$. With the increase of the force a polariton “trace” is formed and at $F_0 = 13$ meV/mm the length of the trace reaches $\approx 3.5 \times 10^3 \Delta x \approx 500 \mu$m (Fig. 2b).

To characterize the steady-state polariton distribution in details we plot in Fig. 2d the polariton BEC density at $y = y_0$ that is, a cross-section of Fig. 2a-c along the line passing through the center of the excitation spot. The inset in Fig. 2d shows that for the force $F_0 = 13$ meV/mm, the maximum of the polariton density is shifted from the center of the excitation spot $x_0$ to $x \approx 1620 \Delta x$.

To prove that the shift of the density maximum is caused by the interaction of the polaritons with the exciton cloud, we investigated evolution of the polariton density with changes of the maximum effective interaction strength $U_0$. Fig. 3a demonstrates changes in the dimensionless polariton density along the line $y = y_0$ with the rise of $U_0$ from 1 meV through 3 meV. It is seen that the position of the maximum of the density is shifted from $x \approx 1500 \Delta x$ at $U_0 = 1$ meV to $x \approx 1620 \Delta x$ at $U_0 = 3$ meV. Fig. 3b-d shows the contour lines for the polariton density $n(r)$ for different $U_0$. From Fig. 3b it is evident that at $U_0 = 2$ meV and $y = y_0 = 1500 \Delta x$ the spatial polariton distribution has **two maxima** positioned at $x \approx 1500 \Delta x$ and $1620 \Delta x$. While increasing $U_0$ to 2.5 meV the left maximum disappears and the right maximum becomes more pronounced, as seen in Fig. 3c. With the further increase of $U_0$, most polaritons are concentrated around the maximum at $x \approx 1620 \Delta x$ (Fig. 3d).

To clarify the reasons for the shift of the density maximum while $U_0$ is increased, we compare in Fig. 3 the distribution of the polariton flux in a steady state $j(r) = (\hbar/2im) (\Psi^*(r) \nabla \Psi(r) - \Psi(r) \nabla \Psi^*(r))$ for different forces. For $F_0 = 0$ the flux $j(r)$ is distributed symmetrically around the center of the excitation spot. As is seen in Fig. 3b the magnitude of the flux, $j$, reaches its maximum at the distance $\sim 120 \Delta x$ from the excitation spot center $r_0$. The presence of the maximum of $j$ at certain distance from the point $r_0$ can be understood if one considers the creation and propagation of polariton wave packets in the potential energy profile.

FIG. 2: (a-c) Evolution of a trace of the long-lifetime polariton BEC with increasing the force $F_0$ for $t = 4800 \Delta t$ and $U_0 = 3$ meV. The colorbars show the dimensionless BEC density $n(r) \Delta x^2$. (d) Evolution of a steady-state polariton density at $y = y_0$ for $U_0 = 3$ meV with increasing $F_0$ shown in a logarithmic scale and in a linear scale in the region around the excitation spot (inset).
In this case, most of the polaritons move in the direction of the force \( F_{\text{ex-pol}}(r) \). The polaritons are accelerated due to the force \( F_{\text{ex-pol}}(r) = -\nabla U_{\text{ex-pol}}(r) \) and hence, their velocity \( v \) gradually rises with the distance from the center. At large distances, the velocity \( v \) tends to a constant because the force \( F_{\text{ex-pol}}(r) \) vanishes. On the other hand, the polariton density \( n(r) \) falls at large distances from \( r_0 \) due to spreading of the polaritons over the sample. In effect, the flux \( j = n v \) reaches the maximum at a certain distance \( \sim a \) from the excitation spot center.

\[ U_{\text{ex-pol}}(r) \]. This results in the shift of the maximum of the polariton density from the spot center, in agreement with Fig. 1d and Fig. 3. It is worth noting that at distances \( \sim a \) from the excitation spot center there is a finite flux directed opposite to the external force \( F_0 \). However, these polaritons eventually flow around the excitation spot and, at large distances from the spot, move in the direction of the force in agreement with the observations in Ref. 21.

**FIG. 3:** (a) Changes in the polariton density at \( y = y_0 \) with the increase of \( U_0 \) from 1 meV to 3 meV for \( t = 5.8 \times 10^3 \Delta t \). (b-d): Contour plots for the polariton density for \( U_0 = 2 \) (b), 2.5 (c), and 3 meV (d); other parameters are the same as in plot (a). The contour lines are labeled with the values of the density \( n(r) \Delta x^2 \). In plot (b) the area with \( n(r) \Delta x^2 \geq 0.52 \) is gray-shaded.

**FIG. 4:** Polariton flux \( j \) for \( U_0 = 3 \) meV, \( t = 5.6 \times 10^3 \Delta t \). The length of the arrows is proportional to the magnitude of the flux \( |j| \). The point at \( r_0 = (1500\Delta x, 1500\Delta x) \) marks the center of the pumping spot.

In the presence of a force \( F_0 \), the polariton flux distribution acquires a strongly asymmetric form. The result of the simulations for \( F_0 = 3 \) meV/mm and \( U_0 = 3 \) meV is shown in Fig. 4. The simulations for other forces \( F_0 \) and energies \( U_0 \) resulted in the polariton flux distributions, which were similar to that shown in Fig. 4. In this case, most of the polaritons move in the direction of the force \( F_0 \).

**FIG. 5:** (a) Variation of the density of a long-lifetime polariton BEC in a microcavity with embedded graphene with rising the gap energy \( \delta \). (b) Points: dependence of the polariton BEC density at the point \( r = (2000\Delta x, 1500\Delta x) \) (marked by a vertical arrow in plot (a)) with changing \( \delta \). Vertical errorbars show uncertainty due to small time-dependent oscillations of the polariton density about the mean values. The dashed curve is a guide to the eye. \( F_0 = 13 \) meV/mm and \( U_0 = 5 \) meV for both plots (a) and (b).

**B. Polariton BEC dynamics in a microcavity with embedded graphene**

Within the same approach, we also studied the propagation of polaritons in a semiconductor microcavity with gapped graphene embedded into it. First, we consider the case of the GaAs-based microcavity, for which we set \( \varepsilon = 13 \). The effective mass \( m \) of the polaritons and the polariton-polariton interaction strength \( g \) have been
found from Eqs. (7)–(11) for different values of the gap energy \( \delta \). The results of the simulations for graphene in Fig. 5 shows that the polariton density in the trace gradually increases with rising the gap energy. To characterize the increase of the polariton BEC density in the trace with changing the gap energy we present in Fig. 6, the dependence of the dimensionless polariton density at the point \( r_1 = (2000\Delta x, 1500\Delta x) \) on the gap energy \( \delta \). The point \( r_1 \) is positioned at the distance of \( 500\Delta x \approx 75 \, \mu m \) from the excitation spot center \( r_0 \). The position of the point \( r_1 \) is marked by a vertical arrow in Fig. 5. Fig. 6 shows that the polariton density at the point \( r_1 \) increases in \( 10.2x \), from \( n \approx 0.013\Delta x^{-2} \) to \( n \approx 0.133\Delta x^{-2} \), with changing \( \delta \) from 0.1 eV to 0.5 eV. Additionally, the shift of the density maximum in the direction of the external force \( F_0 \) is more pronounced for larger \( \delta \), as shown in Fig. 5.

The microcavity can be synthesized from different semiconductor materials. To study the effect of the microcavity material we investigated the propagation of the long-lifetime polariton BEC in graphene in microcavities formed by semiconductor materials CuBr, ZnSe, CdTe, and ZnO \[11\] that is, by those materials, which were utilized for the experimental studies of microcavity polaritons \[16, 17, 25, 42–47\]. According to Eqs. (7)–(11), changes in the dielectric constant \( \varepsilon \) of the microcavity result in the variations of the microcavity length \( L_c \), for which the cavity photons and excitons in graphene are in the resonance, as well as in the changes in the polariton effective mass \( m \) and the polariton interaction strength \( g \).

It was found that the BEC density distributions for CuBr \( (\varepsilon = 5.7) \), ZnSe \( (\varepsilon = 9.1) \), CdTe \( (\varepsilon = 10.2) \) and ZnO \( (\varepsilon = 10.8) \) microcavities are qualitatively similar to those obtained for the microcavity synthesized from GaAs and considered above in this Section. To characterize the details of the changes in the polariton BEC distribution in those microcavities, we plot in Fig. 6 the dependence of the dimensionless density of the condensate, \( n(r)\Delta x^2 \), at the point \( r_1 = (2000\Delta x, 1500\Delta x) \), similarly to that shown in Fig. 5 for a GaAs-based microcavity. It is seen in Fig. 6 that the polariton density at the distance \( \sim 75 \, \mu m \) from the excitation spot center gradually decreases with the decrease of the dielectric constant of the microcavity material. However, this variation is slow: the change of the dielectric constant from \( \varepsilon = 13 \) (GaAs) to 5.7 (CuBr) only results in \( \sim 19\% \) decrease of the BEC density from \( n \approx 0.133\Delta x^{-2} \) to \( n \approx 0.108\Delta x^{-2} \). Thus, the BEC density in a polariton trace in a microcavity with embedded graphene at large distances from the excitation spot is higher for the microcavity with high dielectric constant.

In Ref. [34] it was shown that the Kosterlitz-Thouless transition temperature \( T_c \) for polaritons in a microcavity with embedded graphene increases with the decrease of the microcavity dielectric constant \( \varepsilon \). On the other hand, from the consideration above it follows that the increase of \( \varepsilon \) leads to higher BEC densities at a large distance from the excitation spot. These conclusions are consistent with each other because Ref. [34] describes the redistribution of the polaritons in the superfluid between the normal and superfluid components at finite temperature, whereas in the present work we consider the dynamics of the system at a given total number of the polaritons in the BEC in the low temperature limit \( T \ll T_c \).

C. Effect of the polariton lifetime on the BEC dynamics

Finally, to demonstrate the effect of the polariton lifetime on the BEC dynamics, we studied the BEC spreading in a semiconductor quantum well in a microcavity for traditional, short-lifetime polaritons, for which we took \( \tau = 3 \, \text{ps} \). In Fig. 7, we compare the BEC density for the short-lifetime polaritons in a microcavity with GaAs QW with that for the long-lifetime polaritons in a microcavity with GaAs QW and with embedded graphene at \( \delta = 0.5 \, \text{eV} \). It is clearly seen that for the short-lifetime polaritons, even in the presence of an external force, the BEC is mostly located in the region where it is directly excited by the external pumping and its density rapidly decreases at large distances from the excitation spot. Fig. 7 also shows that the long-lifetime polariton BEC density in graphene with \( \delta = 0.5 \, \text{eV} \) is higher than that in the GaAs quantum well in a microcavity at large distances from the excitation spot.

D. Comparison of the BEC propagation in microcavity with an embedded quantum well and graphene

From the results obtained in Sec. IV A, IV C it follows that the propagation dynamics of the long-lifetime polariton BEC in a microcavity with an embedded GaAs quantum well and in a microcavity formed by GaAs, ZnSe, CdTe, and CuBr with an embedded graphene layer are quantitatively similar to each other. However, the polariton BEC density in the trace for a GaAs-based microcavity with embedded graphene at \( \delta = 0.5 \, \text{eV} \) is higher.
GaAs-based microcavity with \( \tau \) for \( U \) of the gap energy sharply increases with the rise as shown in Fig. 5b. This allows one to utilize the gap energy in graphene as a parameter that controls the polariton BEC propagation in a microcavity. The polariton BEC density far from the excitation spot gradually decreases with the decrease of the dielectric constant of the microcavity material, thus semiconductors with higher dielectric constant provide better conditions for the observation of the polariton BEC propagation.

V. CONCLUSION

Through simulations of the exciton polariton BEC dynamics by using the non equilibrium Gross-Pitaevskii equation, we demonstrated that the long-lifetime (\( \tau \sim 100 \) ps) polaritons in a wedge-shaped microcavity can propagate over a macroscopically long distance \( \sim 500 \) \( \mu \)m. This distance is large compared to that for short-lifetime polaritons in traditional experiments [8, 9, 16, 19, 48]. The maximum of the polariton density in the BEC is shifted from the center of the excitation spot in the direction of the external force due to the exciton-polariton interaction.

We also proposed to observe a polariton BEC propagation in a microcavity with an embedded gapped graphene layer. It was found that the BEC density at large distances from the excitation spot in a semiconductor quantum well and in gapped graphene are comparable with each other. However, in graphene there is an additional parameter that controls the long-lifetime polariton propagation, which is the energy of a gap in the electron and hole energetic spectra. The obtained results can be useful for practical applications of coherent polariton flow in a high-quality microcavity in working elements of integrated optical circuits [4, 48]. The advantage of graphene in a microcavity is that the propagation of a polariton BEC is dynamically tunable via electrostatic gating.

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