Partially ionized atmospheres of neutron stars
with strong magnetic fields

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Abstract

We construct hydrogen atmosphere models for strongly magnetized neutron stars in
thermodynamic equilibrium, taking into account partial ionization. The presence of
bound states affects the equation of state, absorption coefficients, and polarizability
tensor of a strongly magnetized plasma. Therefore the partial ionization influences
the polarization vectors and opacities of normal electromagnetic waves, and thus the
spectra of outgoing radiation. Here we review a model suitable for the most typical
neutron-star atmospheres and focus on the problems that remain to be solved for
its extension to other atmospheric parameters.

Key words: stellar atmospheres, neutron stars, strong magnetic fields

1 Introduction

Thermal emission from neutron stars (NSs) may potentially be used to directly
measure the NS surface magnetic field, temperature, and composition, achieve
a more complete understanding of the evolution of the NSs, and constrain
the properties of matter and physical processes under extreme conditions. It
was realized long ago that a NS atmosphere model should properly include a

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strong magnetic field and partial ionization (see, e.g., Pavlov et al., 1995, for an early review). Models of fully ionized NS atmospheres with strong magnetic fields were constructed by several research groups (e.g., Shibanov et al., 1992; Zane et al., 2000; Ho and Lai, 2003, and references therein). The most recent papers highlighted the effects that may be important for the atmospheres of magnetars: the ion cyclotron feature (Ho and Lai, 2001; Zane et al., 2001) and vacuum polarization effects, including a conversion of the normal modes of radiation propagating in the magnetized atmosphere (Ho and Lai, 2003; Lai and Ho, 2002, 2003).

Early considerations of partial ionization in the magnetized NS atmospheres (Miller, 1992; Rajagopal et al., 1997; also reviewed briefly by Zavlin & Pavlov, 2002) were not very reliable because of oversimplified treatments of atomic physics and nonideal plasma effects in strong magnetic fields. At the typical NS atmosphere parameters, the effects of thermal motion of the bound species are important. In the 1990s, binding energies and radiative transition rates with allowance for the motion effects in strong magnetic fields have been calculated for the H atom (Potekhin, 1994; Potekhin and Pavlov, 1997). Recently these atomic data have been implemented in calculations of thermodynamic functions (Potekhin et al., 1999; Potekhin and Chabrier, 2003, 2004), radiative opacities (Potekhin and Chabrier, 2003, 2004), and spectra (Ho et al., 2003, 2004) of the partially ionized H atmospheres of the NSs. Some results have been presented at the previous COSPAR meeting (Ho et al., 2004a). Now our atmosphere model has been complemented by the effects of the bound states on the polarization properties of the strongly magnetized plasma (Potekhin et al., 2004). Below we briefly summarize the results that allow us to calculate realistic X-ray spectra of thermal radiation from hydrogen NS atmospheres with magnetic fields $B \sim 10^{12} - 10^{14}$ G and effective temperatures $T \gtrsim 10^{5.5}$ K, and outline the problems that remain to be addressed at other atmospheric parameters and compositions.

2 The atmosphere model

We use the equation of state (EOS) for H in strong magnetic fields (Potekhin et al., 1999) based on the free-energy minimization method, which ensures the thermodynamic consistency and allows one to determine number fractions of chemical species, required for opacity calculations. The model takes into account all available theoretical results on the moving H atoms and nonideal Coulomb plasmas in the magnetic fields. This EOS has been tabulated and employed for calculation of opacities for astrophysical use (Potekhin and Chabrier, 2003, 2004).

It is well known that under typical conditions (e.g., far from the resonances)
Fig. 1. Opacities $\kappa_j$ (Eq. [1]) in the O-mode (left panels) and X-mode (right panels) versus photon energy in the hydrogen plasma at $B = 10^{13}$ G, $T = 10^{5.5}$ K, and $\rho = 1$ g cm$^{-3}$, for $\theta_B = 10^\circ$ (upper panels) and $45^\circ$ (lower panels). Solid lines: a self-consistent calculation for a partially ionized plasma (70% of neutrals); dot-dashed lines: the model of full ionization.

radiation propagates in a magnetized plasma in the form of two normal modes, called the extraordinary (X) and the ordinary (O). The opacity in the mode $j$ ($j=$X,O) depends on the photon frequency $\omega$, magnetic field $B$, density $\rho$, temperature $T$, and the angle $\theta_B$ between the magnetic field and propagation direction. It can be written as

$$\kappa_j(\omega, \theta_B) = \sum_{\alpha=-1}^{1} |e^j_{\alpha}(\omega, \theta_B)|^2 \tilde{\kappa}_\alpha(\omega),$$

(1)

where $e^j_{\alpha}$ ($\alpha = -1, 0, 1$) are the cyclic coordinates of the polarization vectors of the normal modes, and the quantities $\tilde{\kappa}_\alpha$ ($\alpha = -1, 0, 1$) do not depend on $\theta_B$. 


Potekhin and Chabrier (2003) calculated $\hat{\kappa}_\alpha(\omega)$ and evaluated $\kappa_j(\omega, \theta_B)$ using the polarization vectors of the normal modes in the fully ionized plasma. Such a calculation (dubbed “hybrid” in Potekhin et al. 2004) was employed in our previous model of partially ionized hydrogen atmospheres of the NSs with strong magnetic fields (Ho et al., 2003, 2004a).

In the new model (Potekhin et al. 2004), we take into account the influence of the bound species on the polarization vectors of the normal modes, making use of the Kramers-Kronig relation\(^2\) between the imaginary and real parts of the plasma polarizability. Thus the calculation of the polarization vectors and opacities of the normal modes has become self-consistent. The calculations of thermal spectra of the NSs show that such self-consistent treatment is necessary if the number fraction of the bound states exceeds several percent. In Fig. 1 we compare radiative opacities calculated with and without allowance for the bound species for one particular set of plasma parameters, typical near the radiative surface of a moderately cool neutron star with magnetic field $B = 10^{13}$ G, for two $\theta_B$ values. In the case shown in the figure, the neutral fraction is 70%, thus the self-consistent treatment of the opacities is important.

3 Conclusion and unsolved problems

The constructed atmosphere models allow us to calculate realistic spectra of thermal X-ray radiation from H atmospheres of the NSs with $10^{12} \lesssim B \lesssim 10^{14}$ G and $T \gtrsim 10^{5.5}$ K. Examples of these spectra are presented elsewhere (Potekhin et al., 2004). There remain the following unsolved problems that prevent us from making similarly reliable calculations beyond these limits.

1. Although the H EOS and opacities have been calculated for $B$ up to $10^{15}$ G and implemented in the atmosphere model (Ho et al., 2003, 2004a), the calculated spectra at $B \gtrsim 10^{14}$ G depend on the adopted model of mode conversion due to the vacuum resonance and on description of propagation of photons with frequencies below the plasma frequency. Both these problems have not been definitely solved. Their solution is also important for modeling the low-frequency (UV and optical) tail of the spectrum.

2. At lower $T$ or higher $B$, H atoms recombine in $H_n$ molecules and eventually form the condensed phase (Lai, 2001, and references therein). Corresponding quantum-mechanical data are very incomplete.

\(^2\) Previously this relation has been used by Bulik & Pavlov (1996) for a neutral gas of H atoms in a strong magnetic field.
3. At $10^9 \, G \lesssim B \lesssim 10^{11} \, G$, transition rates of the moving H atom have not been calculated previously because of their complexity. The first calculation of the energy spectrum appropriate in this range of $B$ has been published when the present paper was in preparation \cite{Lozovik:2004}.

4. At present it is not possible to calculate accurate atmospheric spectra at $B \gtrsim 10^{12} \, G$ for chemical elements other than hydrogen, because of the importance of the effects of finite nuclear mass in the strong field regime. Apart from the H atom, these effects have been calculated only for the He atom at rest \cite{Al-Hujaj:2003a} and for the He$^+$ ion \cite{Bezchastnov:1998}.

5. A more rigorous treatment of radiative transfer in the atmosphere requires solving the transfer equations of the Stokes parameters (see, e.g., \cite{Lai:2003} for the cases of fully ionized atmospheres). However, since the nonorthogonal features of the modes due to neutral species are diminished by the center-of-mass motion, the effect is expected to be small.

Finally, let us note that the atmosphere model presented here, together with a model of radiation from the condensed magnetic surface \cite{vanAdelsberg:2004}, has been successfully used for fitting the spectrum of the isolated neutron star RX J1856.5$-3754$ \cite{Ho:2004}. 

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