Exploring $0\nu\beta\beta$ and Leptogenesis in the Alternative Left-Right Model

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Abstract

We investigate the possibility of neutrinoless double beta decay ($0\nu\beta\beta$) and leptogenesis within the Alternative Left-Right Model (ALRM). Unlike the usual left-right symmetric model, ALRM features a Majorana right-handed neutrino which does not carry any charge. Further, in this picture the down-type quark and the charged leptons receive mass through the additional left-handed scalar field, rather than the usual doublet. Together, these features conspire to generate significant contributions to the $0\nu\beta\beta$ through vector-scalar ($WH$) mediation. For moderate masses of the relevant charged Higgs boson ($M_{H^±} \sim 200$ GeV), the half-life of $T_{1/2}^{WH}$ is $\sim 3 \times 10^{26}$ yrs for both the case of $^{76}$Ge and $^{136}$Xe, well within the sensitivity expected by future experiments. Invoking the resonant leptogenesis, CP violation arising from the right-handed neutrino decay could be the required order to generate the correct baryogenesis, $\epsilon \sim 10^{-6}$, for small Dirac phases and without any fine tuning.

1 Introduction

Neutrinos distinguished as an exclusively left chiral species in the electroweak interactions have provided an intriguing insight into the structure of fundamental interactions. The observation of neutrino oscillations, confirmed over several decades has signalled a key role for them, both in the flavour puzzle and in the understanding of conservation of baryon ($B$) and lepton ($L$) numbers, the global quantum numbers of the low energy Standard Model (SM). Study of such phenomena in turn can provide crucial hints towards a more complete and perhaps also a more elegant theory of elementary particles. Perhaps the most notable among these hints comes from the see-saw mechanism, linking the minuscule mass scale of the observed neutrinos to the grand unification scale, independently suggested by the running of the gauge coupling constants. In all of the popular avatars of the see-saw mechanism, the appearance of newer right handed neutrino type species, and inter alia, the possibility of Majorana mass terms, is inevitable. The possibility of Majorana neutrinos gives rise to the neutrinoless double beta decay ($0\nu\beta\beta$) which has been pursued theoretically, and

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explored experimentally for many decades now. Further, this possibility invariably violates $L$, providing a natural way to address another intriguing issue in particle physics, the matter-anti-matter asymmetry of the Universe, by a mechanism known as leptogenesis.

The observation of the proposed $0\nu\beta\beta$ will be a direct indication of Lepton Number Violation (LNV), and can deliver information regarding the absolute mass scale of the neutrino species. Such LNV processes could arise due to the well explored mechanism with exchange of light Majorana neutrinos, but equally well from some new physics contribution, depending upon the beyond Standard Model (BSM) framework. Thus the study of this phenomenon provides crucial hints to constructing BSM. Among the various BSM frameworks, a minimal one incorporating right handed neutrinos and partially achieving the goals of unification is the class of left-right symmetric models (LRSM). Extensive reviews on $0\nu\beta\beta$ decays in context of LRSM framework can be found in [1] [2] [3] [4] [5] [6] [7] [8] [9] [10] [11] [12] [13] [14] [15] [16].

In the usual versions of the LRSM, the right-handed down-type quark teams up with the right-handed up-type quark to form a doublet under $SU(2)_R$. Similarly, the right-handed electron pairs with the newly introduced right-handed neutrino to form a doublet under $SU(2)_R$. This scenario requires a triplet scalar field whose vacuum expectation value (VEV) provides the Majorana mass for the right-handed neutrino, as needed by the seesaw mechanism [13] [17]. Since the simplest grand unified theory (GUT) based on $SU(5)$ has not been borne out by experiments, and in view of the massive nature of neutrinos, it has been natural to look to the left-right paradigm and any framework that can accommodate it in a fully unified model. All such grand unified theories naturally connect leptons and quarks. Grand unified theories originating from $E_6$ gauge group [18] [19] [20], embed a subgroup $SU(2)_L \times SU(2)_R \times U(1)$ with fermionic content capable of being identified with the proposed LRSM class of models. However, an alternate charge assignment of the fermions in $E_6$ can lead to significant changes in the physical spectrum and the dynamics at low energies. For a more complete description of the model one may refer to [21] [22] [23]. We shall refer to this as Alternative Left-Right Model (ALRM) [24] [25].

This model provides rich neutrino phenomenology. Several additional neutrino states are natural candidates for sterile neutrinos [26]. In the usual LRSM, the important contribution to $0\nu\beta\beta$ decay comes from the $WW$ fusion channel production of the doubly charged scalar boson, which further decays to two electrons. In contrast, in the ALRM there are doublet scalar fields instead of the triplets. The peculiar partnership of the usual right-handed fermions (up type quarks and the charged leptons) with the exotic fermions leads to different constraints on the Yukawa couplings and VEVs. A consequence of these assignments is that some of the Yukawa couplings are significantly larger than in the case of LRSM, generating potentially significant contributions to the $0\nu\beta\beta$ decay through charged Higgs exchange processes. Another important difference from the LRSM is that in the new set up, the right-handed gauge bosons do not couple the usual $\nu_{\tau R}$ and $d_{R}$, meaning that $W_R$ does not contribute to $0\nu\beta\beta$ decay. In this paper, we study such new physics contributions delivering sizable $0\nu\beta\beta$ estimation in context of ALRM framework.

Further, LNV is one of several broad paradigms for understanding the matter-anti-matter asymmetry of the Universe, generally dubbed baryon asymmetry of the Universe (BAU). The Majorana nature of the right-handed neutrino allows the possibility of leptogenesis. Again, the dynamics here is completely unlike the case of LRSM. First, there is no influence of the SM Higgs boson and the CP-asymmetry arises entirely from the decay of right-handed neutrinos and partially achieving the goals of unification is the class of left-right symmetric models (LRSM). The observation of the proposed $0\nu\beta\beta$ will be a direct indication of Lepton Number Violation (LNV), and can deliver information regarding the absolute mass scale of the neutrino species. Such LNV processes could arise due to the well explored mechanism with exchange of light Majorana neutrinos, but equally well from some new physics contribution, depending upon the beyond Standard Model (BSM) framework. Thus the study of this phenomenon provides crucial hints to constructing BSM. Among the various BSM frameworks, a minimal one incorporating right handed neutrinos and partially achieving the goals of unification is the class of left-right symmetric models (LRSM). Extensive reviews on $0\nu\beta\beta$ decays in context of LRSM framework can be found in [1] [2] [3] [4] [5] [6] [7] [8] [9] [10] [11] [12] [13] [14] [15] [16].

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We explore these novel features originating in the alternate $E_6$ as possible explanations of two of the pressing puzzles of phenomenology. The article is organized as follows. In section 2 we discuss the ALRM with its origins in $E_6$ and the existing constraints on the relevant couplings and masses. In section 3 we move on to the calculations of $0\nu\beta\beta$ decay. There we present the possible channels and estimate their contribution identifying the important ones. In section 4 we discuss the leptogenesis, computing the CP-asymmetry arising from the decay of right-handed neutrinos in this model. We summarize our finding and present our conclusions in section 5.
2 The alternative left-right model (ALRM)

It is natural to seek embedding of the rank 5 group LRSM in Spin(10) which happens minimally, with an elegant assignment of fermions to the spinor 16. Later, it was realized in the context of superstring theory that Spin(10) in turn needs to be embedded in $E_6$ (see [18] for a review). However, it was further noted by Ma [20] that an alternative embedding of low energy fermions in the representation 27 is also possible. In this scenario, instead of partnering with the right-handed down-type quark, the right-handed up-quark joins with a new exotic colored fermion, $d'_R$ (of the same charge as $d_R$), to form a doublet under the $SU(2)_R$. Similarly, the right-handed charged leptons partner with a new neutral fermion $(n_R)$ to form a doublet under the same $SU(2)_R$. The right-handed down-type quark, $d_R$ and the right-handed neutrino, $\nu_R$, along with the left-handed degrees of freedom of the newly introduced fermions, $d'_L$ and $n_L$, remain singlets under both $SU(2)_L$ and $SU(2)_R$. The model provides several additional neutrino states as natural candidates for sterile neutrinos [20]. Without supersymmetry, the model can provide two scenarios for neutrino dark matter [25]. For this, an additional $S$-symmetry is imposed, under which the lepton number is either $L = S - T_{3R}$, in the Dark Left-Right Model (DLRM) [27], or $L = S + T_{3R}$, in the Dark Left-Right Model 2 (DLRM2) with a global $U(1)_S$ [28], duly extended to a local $U(1)_S$ in [29]. Finally, it was shown that the partner of the right-handed electron, the scotino, is a viable DM candidate, consistent with all constraints, within suitable parameter space region [21], and the model implications at colliders was explored. In this work, we shall work within the DLRM2, with global $S$ charge assignments as in [30] [23] [23]. With the right-handed neutrinos having $S = 0$, there is a Majorana particle in the spectrum.

The ALRM, arises from the breaking of $E_6$ starting with a substantially different embedding of the low energy fermion representations, and we shall refer to the symmetry of the resulting intermediate scale model as $SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$, to distinguish it from the traditional LRSM. Along with this gauge group we consider DLRM2 type global $U(1)_S$ for the three generations of fermions, and several Higgs fields with the assigned charges as in table [1]. Here $d'$ and $n_{L,R}$ are exotic quarks and leptons, emerging from breaking of $E_6$.

With these assignments, the model Lagrangian includes, in addition to the standard gauge invariant kinetic terms for all fields, a Yukawa interaction Lagrangian $\mathcal{L}_Y$, a Majorana mass term $\mathcal{L}_M$, and a scalar potential $V_H$, for both the bidoublet and the left and right doublet fields, $\chi_L$ and $\chi_R$. Accordingly, the Yukawa Lagrangian and the Majorana mass terms in our model are given by

$$
-\mathcal{L}_Y = \bar{Q}_L Y^d \Phi Q_R + \bar{Q}_L Y^e \chi_L d_R + \bar{Q}_R Y^\nu \phi^L \nu_R + \bar{L}_L Y^d \Phi L_R + \bar{L}_L Y^\nu \phi^L \nu_R + \bar{R}_R Y^\nu \phi^L \nu_R + \text{h.c.},
$$

$$
-\mathcal{L}_M = m_N \bar{\nu}_R \nu_R
$$

where all the generation indices have been omitted for simplicity. The Yukawa couplings $Y$ are $3 \times 3$ matrices with generation labels as indices. Likewise, the most general Higgs potential $V_H$ is given by

$$
V_H = -\mu_1^2 \text{Tr}[\Phi^\dagger \Phi] + \lambda_1 (\text{Tr}[\Phi^\dagger \Phi])^2 + \lambda_2 \text{Tr}(\Phi^\dagger \Phi) \text{Tr}(\Phi^\dagger \Phi)
- \mu_2^2 [\chi_L^\dagger \chi_L + \chi_R^\dagger \chi_R] + \lambda_3 (\chi_L^\dagger \chi_L)^2 + (\chi_R^\dagger \chi_R)^2 + 2\lambda_4 (\chi_L^\dagger \chi_L) (\chi_R^\dagger \chi_R)
+ 2\alpha_1 \text{Tr}[\Phi^\dagger \Phi] [\chi_L^\dagger \chi_L + \chi_R^\dagger \chi_R] + 2\alpha_2 [\chi_L^\dagger \Phi^\dagger \Phi + \chi_R^\dagger \Phi^\dagger \Phi]
+ 2\alpha_3 [\chi_L^\dagger \Phi^\dagger \Phi + \chi_R^\dagger \Phi^\dagger \Phi] + \mu_3 [\chi_L^\dagger \chi_R + \chi_R^\dagger \chi_L],
$$

containing bilinear, trilinear and quartic contributions. In the above expressions, the $SU(2)$ duals of the scalar fields are defined as

$$
\tilde{\chi}_{L(R)} = i\sigma^2 \chi_{L(R)}; \quad \Phi = \sigma^2 \Phi \sigma^2 = \begin{pmatrix} \phi^0_2 & -\phi^1_2 \\ -\phi^1_2 & \phi^0_2 \end{pmatrix}
$$

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$$

with generation labels as indices.
### Fields

| $SU(3)_c \times SU(2)_L \times SU(2)_R' \times U(1)_{B-L}$ | $S$ |
|---|---|
| $Q_L = \begin{pmatrix} u_L \\ d_L \end{pmatrix}$ | $(3, 2, 1, \frac{1}{2})$ | 0 |
| $Q_R = \begin{pmatrix} u_R \\ d'_R \end{pmatrix}$ | $(3, 1, 2, \frac{1}{2})$ | $- \frac{1}{2}$ |
| $d'_L$ | $(3, 1, 1, -\frac{1}{2})$ | $-1$ |
| $d_R$ | $(3, 1, 1, -\frac{1}{2})$ | 0 |
| $L_L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$ | $(1, 2, 1, -\frac{1}{2})$ | 0 |
| $L_R = \begin{pmatrix} n_R \\ e_R \end{pmatrix}$ | $(1, 1, 2, -\frac{1}{2})$ | $+ \frac{1}{2}$ |
| $n_L$ | $(1, 1, 1, 0)$ | $+ 1$ |
| $\nu_R$ | $(1, 1, 1, 0)$ | 0 |
| $\phi = \begin{pmatrix} \phi^0_1 \\ \phi^- \end{pmatrix}$ | $(1, 2, 2^*, 0)$ | $- \frac{1}{2}$ |
| $\chi_L = \begin{pmatrix} \chi^+_L \\ \chi^0_L \end{pmatrix}$ | $(1, 2, 1, \frac{1}{2})$ | 0 |
| $\chi_R = \begin{pmatrix} \chi^+_R \\ \chi^0_R \end{pmatrix}$ | $(1, 1, 2, \frac{1}{2})$ | $+ \frac{1}{2}$ |

Table 1: ALRM particle content, for one generation of fermions and for the Higgs fields with charge assignments under $SU(3)_c \times SU(2)_L \times SU(2)_R' \times U(1)_{B-L}$ (second column) and the global $U(1)_S$ (third column).

where $\sigma^2$ is the Pauli matrix in the standard notation. The vacuum expectation value (VEV) acquired by the neutral component of $\chi_R$ breaks the $SU(2)_R' \times U(1)_{B-L}$ symmetry down to the standard gauge symmetry, which is further broken to the electromagnetic gauge symmetry by the VEVs of the bidoublet and left-handed doublet fields. The VEVs of these fields are given by

$$
\langle \Phi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ k \end{pmatrix}, \quad \langle \chi_L \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_L \end{pmatrix}, \quad \langle \chi_R \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_R \end{pmatrix}.
$$

It is found that the VEV of the other neutral component of the bidoublet, $\phi^0_1$ remains zero [22] which helps to avoid the unwanted mixing between $d$ and $d'$ and also between $\nu_L$ and the scotino $n_R$. This also decouples the $\phi^0_1$ field from the other neutral scalar fields, making its mass eigenstate the same as the gauge eigenstate.
With the complex neutral scalar fields expressed in terms of their real degrees of freedom, the fields are
\[
\phi_1^0 = \frac{1}{\sqrt{2}} \left[ R\{\phi_1^0\} + i \Im\{\phi_1^0\} \right],
\]
\[
\phi_2^0 = \frac{1}{\sqrt{2}} \left[ k + R\{\phi_2^0\} + i \Im\{\phi_2^0\} \right],
\]
\[
\chi_{L,R}^0 = \frac{1}{\sqrt{2}} \left[ v_{L,R} + R\{\chi_{L,R}^0\} + i \Im\{\chi_{L,R}^0\} \right].
\] (6)

Then the massive CP-even Higgs bosons \(H_i^0\) (with \(i = 0, 1, 2, 3\)), the massive CP-odd Higgs bosons \(A_i^0\) (with \(i = 1, 2\)) and the two massless Goldstone bosons \(G_{1,2}^0\) are expressed in terms of the gauge eigenstates, as
\[
R\{\phi_1^0\} = A_1^0, \quad R\{\phi_2^0\} = H_0^0,
\]
\[
\begin{pmatrix}
R\{\phi_2^0\} \\
R\{\chi_L^0\} \\
R\{\chi_R^0\}
\end{pmatrix} =
\begin{pmatrix}
U_{3\times 3}^A \\
G_1^0 \\
G_2^0
\end{pmatrix}
\quad \text{and} \quad
\begin{pmatrix}
R\{\phi_1^0\} \\
R\{\chi_L^0\} \\
R\{\chi_R^0\}
\end{pmatrix} =
\begin{pmatrix}
U_{3\times 3}^H \\
H_0^0 \\
H_2^0
\end{pmatrix}. \quad (7)
\]

We refer to Refs. [21] [22] [23] for details and explicit expressions of the mixing matrices \(U_{3\times 3}^A\) and \(U_{3\times 3}^H\), for the CP-odd and CP-even scalars. Pertinent for our further discussion are the charged scalar bosons and their interaction with the quarks and the leptons. The eight degrees of freedom in the charged scalar sector of the unbroken symmetry, \(\phi_1^\pm, \phi_2^\pm, \chi_L^\pm\) and \(\chi_R^\pm\), mix into two physical massive charged Higgs bosons \(H_1^\pm\) and \(H_2^\pm\), and two massless Goldstone bosons \(G_1^\pm\) and \(G_2^\pm\) that are absorbed by the \(W_L^\pm\) and \(W_R^\pm\) gauge bosons,
\[
\begin{pmatrix}
\phi_1^\pm \\
\chi_L^\pm
\end{pmatrix} =
\begin{pmatrix}
\cos \beta & \sin \beta \\
-\sin \beta & \cos \beta
\end{pmatrix}
\begin{pmatrix}
H_1^\pm \\
G_1^\pm
\end{pmatrix}, \quad \begin{pmatrix}
\phi_2^\pm \\
\chi_R^\pm
\end{pmatrix} =
\begin{pmatrix}
\cos \zeta & \sin \zeta \\
-\sin \zeta & \cos \zeta
\end{pmatrix}
\begin{pmatrix}
H_2^\pm \\
G_2^\pm
\end{pmatrix}. \quad (8)
\]

with
\[
\tan \beta = \frac{k}{v_L} \quad \text{and} \quad \tan \zeta = \frac{k}{v_R}. \quad (9)
\]

Masses of the new physical charged bosons are given in terms of the parameters of the Lagrangian and the VEVs, as
\[
M_{H_1^\pm} = v^2 (\alpha_3 - \alpha_2) - \frac{\mu_3}{\sqrt{2}} \frac{v^2 v_R}{k v_L}, \quad \text{and} \quad M_{H_2^\pm} = (k^2 + v_R^2) (\alpha_3 - \alpha_2) - \frac{\mu_3}{\sqrt{2}} \frac{(k^2 + v_R^2) v_L}{k v_R}. \quad (10)
\]

where \(v^2 = k^2 + v_L^2\). The couplings of these charged scalars within lepton and quark charged currents are relevant when discussing \(0\nu\beta\beta\) and leptogenesis. To obtain these couplings, we examine the Yukawa couplings in more detail. With the charged and neutral scalar degrees of freedom as above, the gauge eigenstates of the bidoublet as well as of the two doublet scalar fields in the unitary gauge can be written in terms of the mass eigenstates as
\[
\Phi = \begin{pmatrix} H_1^0 + i A_1^0 \\ \cos \zeta H_2^+ - k + R\{\phi_2^0\} + i U_{11}^A A_2 \end{pmatrix}, \quad \chi_L = \begin{pmatrix} - \sin \beta H_1^+ \\ \cos \beta \chi_L \\ v_L + R\{\chi_L^0\} + i U_{11}^A A_2 \end{pmatrix}, \quad \chi_R = \begin{pmatrix} - \sin \zeta H_2^+ \\ \cos \zeta H_2^+ \\ v_R + R\{\chi_R^0\} + i U_{31}^A A_2 \end{pmatrix}. \quad (11)
\]
Similarly, the ratio of the VEVs, for the first generation quarks, and different Yukawa couplings: of the light neutrinos, but up and down quarks, and leptons and neutrinos, respectively acquire masses from

\[ Y^e = \frac{\sqrt{2} m_e}{k} \sim 2.93 \times 10^{-6}, \quad Y^\mu = \frac{\sqrt{2} m_\mu}{k} \sim 6.08 \times 10^{-4}, \quad Y^\tau = \frac{\sqrt{2} m_\tau}{k} \sim 1.02 \times 10^{-2}. \]

for the charged leptons. Further, with the light neutrino mass \( m_\nu \sim 0.01 \text{ eV} \) and the heavy neutrino mass \( m_N \sim 10 \text{ TeV} \), the corresponding Yukawa couplings are

\[ Y^\ell = \frac{\sqrt{2} m_\nu m_N}{v_L} \sim 8.96 \times 10^{-5}. \]

Similarly, the ratio of the VEVs, \( \tan \beta = \frac{k}{v_L} \sim \frac{246}{8} \approx 49.2 \). Or,

\[ \cos \beta \sim 0.0203 \quad \text{and} \quad \sin \beta \sim 1. \]
The mixing angles by the electroweak mixing between $A$ can be diagonalized through three rotations that mix the $\nu$ states, but connects the right-handed charged leptons and up-type quarks to $d^p_R$ and $u^p_R$, respectively, the exotic fermions. However, for completeness we briefly discuss gauge boson masses below. As usual, the spontaneous breaking of the left-right symmetry generates the boson masses and possibly induces their mixing. While the charged gauge bosons $W_L$ and $W_R$ could mix in the usual LRSM case, in the ALRM they do not mix as $\langle \phi_0^0 \rangle = 0$. In the present case, their masses are given by

$$M_{W_L} = \frac{1}{2} g_L \sqrt{k^2 + v_R^2} \equiv \frac{1}{2} g_L v \quad \text{and} \quad M_{W_R} = \frac{1}{2} g_R \sqrt{k^2 + v_R^2}.$$  \hspace{1cm} (21)

In the neutral sector, the gauge boson mass-squared matrix is written, in the $(B_\mu, W^3_{L\mu}, W^3_{R\mu})$ basis, as

$$\langle M^0 \rangle^2 = \frac{1}{4} \begin{pmatrix} g^2 - (v_L^2 + v_R^2) & -g_{n-L} g_L v_L^2 & -g_{n-L} g_R v_R^2 \\ -g_{n-L} g_L v_L^2 & g_L^2 v_L^2 & -g_L g_R k^2 \\ -g_{n-L} g_R v_R^2 & -g_L g_R k^2 & g_R^2 (k^2 + v_R^2) \end{pmatrix}.$$  \hspace{1cm} (22)

It can be diagonalized through three rotations that mix the $B$, $W^3_L$ and $W^3_R$ bosons into the massless photon $A$ and massive $Z$ and $Z'$ states,

$$\begin{pmatrix} B_{\mu} \\ W^3_{L\mu} \\ W^3_{R\mu} \end{pmatrix} = \begin{pmatrix} \cos \varphi_w & 0 & -\sin \varphi_w \\ 0 & 1 & 0 \\ \sin \varphi_w & 0 & \cos \varphi_w \end{pmatrix} \begin{pmatrix} \cos \theta_w & -\sin \theta_w & 0 \\ \sin \theta_w & \cos \theta_w & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} A_\mu \\ Z_\mu \\ Z'_\mu \end{pmatrix},$$  \hspace{1cm} (23)

The $\varphi_w$-rotation mixes the $B$ and $W^3_R$ bosons into the hypercharge boson $B'$ and its orthogonal combination as generated by the breaking of $SU(2)_{R'} \times U(1)_{B-L}$ into to the hypercharge group $U(1)_{Y}$. The usual electroweak mixing between $B'$ and $W^3_L$ generating the photon, $A$ and the orthogonal combination is achieved by the $\theta_w$-rotation, and finally the $\theta_w$-rotation is related to $Z - Z'$ mixing, which is strongly constrained. The mixing angles $\varphi_w$ and $\theta_w$ are related to the gauge couplings in a straightforward manner,

$$\sin \varphi_w = \frac{g_{n-L}}{\sqrt{g^2_{n-L} + g^2_n}} = \frac{g_n}{g_L} \quad \text{and} \quad \sin \theta_w = \frac{g_n}{\sqrt{g^2_n + g^2_R}} = \frac{e}{g_L},$$  \hspace{1cm} (24)

where $g_n$ and $e$ denote the hypercharge and electromagnetic coupling constants, respectively. Finally $\theta_w$ depends on the VEVs and the other two mixing angles along with the gauge couplings, as

$$\tan(2 \theta_w) = \frac{2 g_L g_n \cos \varphi_w \cos \theta_w (\cos^2 \varphi_w k^2 - \sin^2 \varphi_w v^2_L)}{g^2_n \cos^2 \theta_w v^2_L - (g^2_n - g^2_R \cos^2 \varphi_w \cos^2 \theta_w) \cos^2 \varphi_w k^2 - (g^2_R - g^2_{n-L} \cos^2 \theta_w \sin^2 \varphi_w) \cos^2 \varphi_w v^2_L}.$$  \hspace{1cm} (25)

As can be seen, $\theta_w$ is negligible for $k \ll v_R$. Neglecting this $Z - Z'$ mixing, the $Z$ and $Z'$ boson masses are given by

$$M_Z = \frac{1}{2} g_L \cos \theta_w v \quad \text{and} \quad M_{Z'} = \frac{1}{2} g_R \sqrt{g^2_{n-L} \sin^2 \varphi_w \cos^2 \varphi_w v^2_L + g^2_n (\cos^4 \varphi_w k^2 + v^2_R)}.$$  \hspace{1cm} (26)

### 2.1 Scalar mass bounds

Before we embark on a detailed analysis of the $0\nu\beta\beta$ in this model, we discuss the limits on the masses of the charged Higgs and gauge bosons in the model. The lightest charged Higgs boson in the ALRM is $H^+_{2\alpha}$, which is long-lived, so that limits on its mass are probed by searches for heavy stable charged particles. The $H^+_{2\alpha}$ bosons are pair-produced via the Drell-Yan mechanism, in proton-proton collisions at centre-of-mass
energies of 7 TeV [31,32], 8 TeV [33] and 13 TeV [34,35,36,37,38,39] and in electron-positron collisions at a centre-of-mass energy of 183 GeV [40].

The LEP results impose strict limits in the [45.9, 89.5] GeV mass range [40]. The searches in 13 TeV LHC collisions exclude signal cross sections ranging from 10 to 100 fb, the exact limit value depending on the model, although direct limits are not straightforward to extract because of modelling of various detector effects which is complicated. Similar conclusions hold for 7 and 8 TeV LHC search results [33,32,31].

The heavier charged Higgs state $H^+_1$ is the one that would be relevant for the $0\nu\beta\beta$ decay. This state would be constrained by more standard searches for additional Higgs states, such as the one of [41]. Those searches are targeting a specific production mode and a given decay channel. For example, Run 2 the analyses in [41,42] investigated the LHC sensitivity to charged Higgs bosons decaying into $H^\pm \rightarrow \tau^\pm \nu_\tau$ [41]. There the results are interpreted within MSSM, and a lower limit $M_{H^\pm} > 160$ GeV is quoted. For heavier $H^\pm_1$ case, the analyses of charged Higgs boson production and decay in a $tb$ final state or heavy Higgs boson production in association with a $tb$ pair or a $W_Lb\bar{b}$ system have also been carried out (see, e.g., refs. [33,34,35]). Limits on cross-sections times branching ratio are again obtained in the context of two benchmarks in the MSSM, again these are difficult to compare with our results since the couplings are completely different.

Unlike in the ordinary LRSM, the charged right-handed gauge boson $W_R$ couples to right-handed up-type quarks and charged leptons and their exotic quarks and scotino partners, rather than the usual right-handed neutrinos and down quarks. In addition, there is no mixing between the SM $W_L$ boson and the its $SU(2)_R$ counterpart. Therefore, the limits on the $W_R$-boson mass, imposed from flavor violation, do not apply here, relaxing considerably constraints on its mass. As the $W_R$ does not affect either $0\nu\beta\beta$ decay or leptogenesis, we do not discuss it further.

3 Neutrinoless Double Beta Decay ($0\nu\beta\beta$) in ALRM

The half-life for various isotopes is related to the matrix elements and phase factor $G$. The matrix element has two parts, one corresponding to the nuclear currents ($M$) and the other corresponding to the leptonic current ($\eta$). The expression for half-life is given by

$$\frac{1}{T_{1/2}^{0\nu\beta\beta}} = \sum_i G_i \left|\eta_i M_i\right|^2$$

(27)

where $i$ corresponds to standard as well as different BSM channels. Up to now, $0\nu\beta\beta$ decay has not been observed. The best half-life limits on $0\nu\beta\beta$ come from experiments on two isotopes, Ge$^{76}$ and Xe$^{136}$. The Heidelberg-Moscow collaboration gives 90% C.L. limit of $T_{1/2}^{0\nu\beta\beta}(^{76}\text{Ge}) > 1.9 \times 10^{25}$ yrs [45], with the latest results on Germanium coming from GERDA [46] and MAJORANA [47] Collaborations quoting $9 \times 10^{25}$ yrs and $2.7 \times 10^{25}$ yrs, respectively. Results from the Xenon experiments on the other hand are given by EXO-200 and KamLAND-ZEN quoting $T_{1/2}^{0\nu\beta\beta}(^{136}\text{Xe}) > 1.8 \times 10^{25}$ yrs [48] and $T_{1/2}^{0\nu\beta\beta}(^{136}\text{Xe}) > 1.07 \times 10^{26}$ yrs [49], respectively, both at 90% C.L.

Some of the relevant channels for $0\nu\beta\beta$ in ALRM are listed in figs. 1 to 3. The usual channel is given in fig. 1(a) with the left-handed neutrinos and $W_L$ propagators. The other diagrams, fig. 1(b), (c), (d) show the scalar-scalar mediated channel with two right-handed electrons in the final state, with the couplings explicitly indicated. Notice that the couplings are related to the mass of quarks and electrons, as given in eq. (15) to eq. (20). It is evident that the scalar mediated combinations are not significant.

In fig. 2 channels with scalar-scalar propagator and two left-handed electrons in the final state are given. Again, we shall see that the contributions due to these diagrams are negligible. On the other hand, the mixed scalar-vector propagator channels with Feynman diagrams in fig. 3 provide larger contributions, with fig. 3(d) contributing at par with the standard case for suitably chosen parameters.
3.1 Amplitudes and parameters for various diagrams contributing to $0\nu\beta\beta$

Before writing down the required expressions for amplitudes and particle physics parameters for the diagrams, we define the transformation relation between flavor and mass eigenstates of neutrinos (both left- and right-handed) as,

$$\nu_{L\alpha} = V_{\nu\nu}^{\alpha i} \nu_i + V_{\nu N}^{\alpha i} N_i,$$

$$\nu_{R\beta} = V_{N\nu}^{\beta j} \nu_j + V_{NN}^{\beta j} N_j,$$

(28)

where $\alpha, \beta$ correspond to flavor indices $e, \mu, \tau$, while $i,j$ represent mass eigenstates 1, 2, 3. Also $V$ denotes the rotation matrix between flavor and mass bases. The estimation for amplitudes as well as dimensionless particle physics parameters in context of various BSM scenarios can be found explicitly in [50, 51, 52, 53].

We divide the different channels into five categories, and we give the expressions for the amplitudes below.

3.1.1 Vector-Vector ($W_L - W_L$) mediated diagrams with $e_L - e_L$ emission

This so-called “standard contribution” in the literature appears in all models allowing for $0\nu\beta\beta$, including that in the usual LRSM [3] and is shown in the Feynman diagram in fig 1(a). The amplitude for this process is given by

$$A_{W_LW_L} \sim G_F^2 \sum_i \left( \frac{V_{\nu e}^{\alpha i} m_{\nu e}}{p^2} - \frac{V_{\nu N}^{\alpha i} m_{\nu N}}{m_{N_i}} \right).$$

(29)

with the corresponding particle physics parameters

$$\eta_{LL,\nu e}^{W_LW_L} = \sum_i \frac{V_{\nu e}^{\alpha i} m_{\nu e}}{m_e}$$

and

$$\eta_{LL,\nu N}^{W_LW_L} = -m_p \sum_i \frac{V_{\nu N}^{\alpha i} m_{\nu N}}{m_{N_i}}.$$

(30)
The amplitude of the scalar-scalar mediated process with right-handed neutrino exchange and the emission of two left-handed electrons, as shown in the Feynman diagrams in fig. 2, is

\[ A_{\sigma,\sigma',\nu_L}^{H_1, H_1} \sim \frac{G_F^2}{g_L^2} \frac{M_W^4}{M_{H_1}^4} \kappa_{ud}^2 (Y^{(2)}_L)^2 \cos^2 \beta \sum_i \left( \frac{\nu_{\alpha i} \nu_{\alpha i}}{m_{\nu_i}} - \frac{\nu_{\alpha i}^N \nu_{\alpha i}^N}{m_{N_i}} \right), \]  

where \( \sigma \) and \( \sigma' \) denote the chirality of the outgoing quarks. The dimensionless particle physics parameters are given by

\[ Y_{\nu_{\alpha i},H_1,H_1}^{\nu_{\alpha i}',H_1,H_1} = \frac{M_W^4}{M_{H_1}^4} \kappa_{ud}^2 (Y^{(2)}_L)^2 \cos^2 \beta \sum_i \frac{\nu_{\alpha i} \nu_{\alpha i}}{m_{\nu_i}} \quad \text{and} \quad \nu_{\alpha i}^N \nu_{\alpha i}^N \sum_i \frac{-m_p \nu_{\alpha i}^N \nu_{\alpha i}^N}{m_{N_i}}. \]  

The coupling combination, \( \kappa_{ud}^2 \), depends on the chirality of the quarks. When both the \( u \) quarks are right-handed it is \( (Y^{(2)}_L)^2 \cos^2 \beta \), and with both left-handed it is \( (Y^{(2)}_L)^2 \sin^2 \beta \), while for the mixed case of one left-handed and one right-handed quark it is \( Y^{(2)}_L Y^{(2)}_R \sin \beta \cos \beta \).

### 3.1.3 Scalar-Scalar (H1 − H1) mediated diagrams with \( \nu_L - \nu_L \) emission

The amplitude of the scalar-scalar mediated process with right-handed neutrino exchange and the emission of two left-handed electrons, as shown in the Feynman diagrams in fig. 2, is

\[ A_{\sigma,\sigma',\nu_L}^{H_1, H_1} \sim \frac{G_F^2}{g_L^2} \frac{M_W^4}{M_{H_1}^4} \kappa_{ud}^2 (Y^{(2)}_L)^2 \sin^2 \beta \sum_i \left( \frac{\nu_{\alpha i}^N \nu_{\alpha i}^N}{m_{\nu_i}} - \frac{\nu_{\alpha i} \nu_{\alpha i}}{m_{N_i}} \right). \]  

Figure 2: Feynman diagrams contributing to the 0νββ. \( H_1 - H_1 \) propagators and left-handed electron emission. The color code is as in [1].
Similar to the previous case, the quark-chirality dependent coupling combination \( \kappa_{ud}^2 \) is \( (Y^q)^2 \cos^2 \beta \) when both \( u \)-quarks are right-handed, \( (Y^q)^2 \sin^2 \beta \) when both are left-handed, and \( Y^q Y^q L^* \sin \beta \cos \beta \) in the mixed case. The dimensionless particle physics parameters for each of these channels (expressed in mass basis) can be written as

\[
\eta_{\sigma,\sigma',H_1} = \frac{M_{W \ell}}{M_{H_1}} \kappa_{ud}^2 (Y^q L^*)^2 \sin^2 \beta g_{L}^2 \sum_i \frac{Y_{\alpha i}^N m_{\nu_i}}{m_e}, \quad \text{and} \quad (34)
\]

\[
\eta_{N_i,\sigma,\sigma',H_1} = \frac{M_{W \ell}}{M_{H_1}} \kappa_{ud}^2 (Y^q L^*)^2 \sin^2 \beta g_{L}^2 \sum_i \frac{-m_p Y_{\alpha i}^N}{m_{N_i}}, \quad (35)
\]

where \( \eta_{\sigma,\sigma',\nu \nu}^{X,H_1} \) denotes the contributions arising due to \( X = \nu_i \) or \( N_i \) exchange in the mass basis.

### 3.1.4 Vector-Scalar \((W_L - H_1)\) mediated diagrams with \( e_L - e_L \) emission

Here, one of the quark currents connected with \( W_L \) is left-handed, while the other current is helicity-flip interacting with the scalar. As discussed in Ref. [50, 51, 52], the amplitude is given by

\[
A_{W \ell H_1} \sim \frac{G_F^2}{g_L} \frac{M_{W \ell}^2}{M_{H_1}} \kappa_{ud} Y^L_{\ell \ast} \sin \beta \sum_i \left( \frac{Y_{\alpha i}^N Y_{\alpha i}^N}{m_{\nu_i}} + \frac{Y_{\alpha i}^N Y_{\alpha i}^N}{m_{N_i}} \right), \quad (36)
\]

where the quark coupling, \( \kappa_{ud} \) is \( Y^q \cos \beta \) when one of the \( u \)-quarks is right-handed, while it is \( Y^q \sin \beta \) when both the \( u \)-quarks are left-handed. The dimensionless particle physics parameters are

\[
\eta_{\sigma,\sigma',\nu \nu}^{X,H_1} = \frac{M_{W \ell}}{M_{H_1}} \kappa_{ud} Y^L_{\ell \ast} \sin \beta g_{L}^2 \sum_i \frac{Y_{\alpha i}^N}{m_{\nu_i}}, \quad \text{and} \quad (37)
\]

\[
\eta_{N_i,\sigma,\sigma',\nu \nu}^{X,H_1} = \frac{M_{W \ell}}{M_{H_1}} \kappa_{ud} Y^L_{\ell \ast} \sin \beta g_{L}^2 \sum_i \frac{Y_{\alpha i}^N Y_{\alpha i}^N}{m_{N_i}} \frac{-m_p Y_{\alpha i}^N}{m_{N_i}}, \quad (38)
\]
3.1.5 Vector-Scalar \((W_L - H_1)\) mediated diagrams with \(e_L - e_R\) emission:

The other two channels in this category are associated with the Feynman diagrams given in fig.3 (c) and (d). This gives the most promising contribution for the ALRM considered here, leading to helicity flipped lepton current. The amplitudes are

\[
A_{\sigma'_{\nu},\nu_L}^{W_L H_1} \sim \frac{G_F}{g_L^2} \frac{M_W^2}{M_{H_1}} \kappa_{ud} Y^I \cos \beta \sum_i \left( \frac{\nu_{\alpha i}^\nu}{\gamma \cdot p} - \frac{\nu_{\alpha i}^{N2}}{m_{N_i}} \right),
\]

with \(\kappa_{ud} = Y^u \cos \beta\) when one of the \(u\)-quarks is right-handed, and \(Y^u \sin \beta\) when both the \(u\)-quark are left-handed. And the corresponding particle physics parameters are

\[
\eta_{\sigma'_{\nu},\nu_L}^{W_L H_1} = \kappa_{ud} Y^I \cos \beta \frac{M_W^2}{g_L^2} \frac{M_{H_1}^2}{M_{H_1}} \sum_i \nu_{\alpha i}^{N2} \gamma \cdot p \frac{m_{N_i}}{m_e}, \quad \text{and}
\]

\[
\eta_{\sigma'_{\nu},\nu_L}^{N_L W_L H_1} = \kappa_{ud} Y^I \cos \beta \frac{M_W^2}{g_L^2} \frac{M_{H_1}^2}{M_{H_1}} \sum_i \nu_{\alpha i}^{N2} \left( \frac{m_p}{m_{N_i}^2} \right).
\]

3.2 Numerical estimates

The dimensionless particle parameters corresponding to different channels depend on the Yukawa couplings, the ratio the VEVs and the neutrino mixing matrix elements. The relevant combinations of Yukawa couplings and ratio of the VEVs, respecting the constraints discussed in section 2, are given in table 2a, while all the mass parameters are given in table 2b. The neutrino mixing matrix elements connect the mass eigenstates to the flavor eigenstates as in eq. (28). In our case only the electron type neutrinos are relevant. Further, we have the unitarity condition

\[
\sum_i \nu_{ei}^{\nu2} = \sum_i \nu_{ei}^{NN2} = 1, \quad \text{(42)}
\]

and we considered

\[
\sum_i \nu_{ei}^{\nu2} m_{\nu_i} \sim 0.01 \text{ eV}, \quad \sum_i \nu_{ei}^{NN2} \frac{m_{N_i}}{m_{N_i}} \sim 0.1 \text{ (TeV)}^{-1}
\]

assuming close degeneracy of the neutrinos. This is easily followed by \(\nu_{ei}^{\nu N} \sim \nu_{ei}^{NN} \sim \left(\frac{m_{\nu}}{m_{N_i}}\right) \nu_{ei}^{\nu2} \sim 10^{-15}\).

We have, therefore, neglected the contributions proportional to \(\nu_{ei}^{NN}\), except when they are the leading contribution. In addition, we have considered the weak coupling constant, \(g_L \sim 0.65\). With these values,
In Table 3, this leads to different isotopes Ge studied in the literature. The corresponding phase space factors and the nuclear matrix elements for two

The best known mechanism leading to

3.3 Calculation of Half-life

The first term corresponds to the standard contribution with $W_L - H_1$ mediated (fig. 1a), which is widely studied in the literature. The corresponding phase space factors and the nuclear matrix elements for two different isotopes Ge$^{76}$ and Xe$^{136}$ [56, 57] are given in Table 4. With the particle physics parameters given in Table 5, this leads to

$$T_{1/2}^{\nu W_\nu} (^{76}\text{Ge}) = (9.82 - 65.09) \times 10^{27} \text{ yrs},$$

$$T_{1/2}^{\nu W_\nu} (^{136}\text{Xe}) = (4.74 - 28.49) \times 10^{27} \text{ yrs},$$

$$T_{1/2}^{\nu W_\nu} (^{136}\text{Xe}) = (4.74 - 28.49) \times 10^{27} \text{ yrs},$$
vector current operators, the only significant contribution is from the leptonic currents can be expressed as

\[ \sum_j \epsilon_j \bar{\psi} \gamma_{\mu} \gamma_5 \psi \times J_\mu, \]

where \( \epsilon_j \) are, respectively. Also this asymmetry is measured relative to the number of photons \( n_\gamma \) which can be extracted from observations and

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|}
\hline
Isotope & \( G_{09} \) (yrs\(^{-1}\)) & \( M_W^{W\nu} \) \\
\hline
Ge – 76 & \( 5.77 \times 10^{-15} \) & \( 2.58 - 6.64 \) \\
Xe – 136 & \( 3.56 \times 10^{-14} \) & \( 1.57 - 3.85 \) \\
\hline
\end{tabular}
\caption{Standard 0\( \nu \beta\beta \) phase space factors \cite{56} and nuclear matrix elements for the different exchange processes \cite{57} used in the analysis.}
\end{table}

where the range corresponds to the range in the NME in table 4. To get an estimate of these factors for the other channels involving the scalar exchange, we turn to the discussion in Ref. \cite{58}. The most general Lorentz invariant Lagrangian can be written in terms of the nuclear and lepton currents as

\[ \mathcal{L} = \frac{G_F^2}{2m_p} \left[ \epsilon_1 J J_j + \epsilon_2 J^{\mu
u} J_{\mu\nu,j} + \epsilon_3 J_\mu J_{\mu,j} + \epsilon_4 J_\mu J_{\mu\nu,j} + \epsilon_5 J_\mu J_{\mu\nu} \right] + \epsilon_6 J^{\mu
u} J_{\mu\nu} + \epsilon_7 J_{\mu\nu} J_{\mu\nu} + \epsilon_8 J_{\mu\alpha} J_{\nu\alpha} J_{\mu
u}, \]

where \( m_p \) is the mass of proton and the scalar, vector as well as tensor currents at the hadronic vertices are given by \( J = \bar{u}(1 \pm \gamma_5)d, \ J^{\mu} = \bar{u}_\gamma \gamma^\mu(1 \pm \gamma_5)d, \ J^{\mu
u} = \bar{u}_\gamma \gamma^\mu(1 \pm \gamma_5)c, \) respectively. The corresponding leptonic currents can be expressed as \( j = \bar{e}(1 \pm \gamma_5)e, \ j^{\mu} = \bar{e} \gamma^\mu(1 \pm \gamma_5)e, \ j^{\mu
u} = \bar{e} \gamma^\mu(1 \pm \gamma_5)e, \) respectively. Also this \( \epsilon's \) are same as our estimated \( \eta's \). In the UV complete scenario that we presented here, there are no tensor operators. As seen from the discussion in section 3.2 among the scalar and vector current operators, the only significant contribution is from the \( W_L - H_1 \) channel with the emission of two electrons with opposite chirality (fig. 3e and fig. 3f). The relevant term in the above Lagrangian corresponding to this contribution is

\[ \mathcal{L} \supset \frac{G_F^2}{2m_p} (\epsilon_5 J_\mu J_{\mu\nu}), \]

with the corresponding phase factor, as in \cite{58}, given by

\[ G_{W_L}^{LR}(\gamma_8, \gamma_6) = \frac{(m_e R)^2}{8} \ G_{09}(\gamma_8, \gamma_6) = 2.66 \times 10^{-14} \text{ yrs}^{-1}, \]

\[ G_{W_L}^{LR}(\gamma_8, \gamma_6) = 1.29 \times 10^{-14} \text{ yrs}^{-1} \]

where we have used \( G_{09}(\gamma_8, \gamma_6) = 3.3 \times 10^{-10} \) and \( G_{09}(\gamma_8, \gamma_6) = 1.6 \times 10^{-9} \) as given in Refs. \cite{58} \cite{59}. The nuclear radius, \( R \) is taken as 10 fm, and \( m_e \) is the mass of electron. The nuclear matrix element for the two elements are, \( M_{M_0}^{WH}(\gamma_8, \gamma_6) = \mp 18.96 \) (denoted as \( M_0 \) in Ref. \cite{58}) and \( M_{M_0}^{WH}(\gamma_8, \gamma_6) = \mp 9.45 \) \cite{59}. This leads to the half-life corresponding to the \( W_L - H_1 \) channel,

\[ T_{\frac{1}{2}, n_{\gamma}}^{0\nu}(\gamma_8, \gamma_6) = 3.6 \times 10^{26} \left( \frac{200 \text{ MeV}}{\gamma \cdot p} \right)^2 \left( \frac{M_{H_1}}{200 \text{ GeV}} \right)^4 \text{ yrs}, \]

\[ T_{\frac{1}{2}, n_{\gamma}}^{0\nu}(\gamma_8, \gamma_6) = 3.0 \times 10^{26} \left( \frac{200 \text{ MeV}}{\gamma \cdot p} \right)^2 \left( \frac{M_{H_1}}{200 \text{ GeV}} \right)^4 \text{ yrs}. \]

These values are one to two orders of magnitude smaller than the standard channel given in eq. (47), while remaining safely within the current experimental limits quoted in the beginning of this section.

4 Leptogenesis in ALRM

Cosmological observations have definitively established the preponderance of matter over antimatter. This asymmetry is measured relative to the number of photons \( n_\gamma \) which can be extracted from observations and
found to be \([60, 61]\)

\[
\Delta B \equiv \frac{n_B - n_{\bar{B}}}{n_\gamma} \sim 10^{-10},
\]

(52)

with \(n_B, n_{\bar{B}}\) being the number of baryons and anti-baryons, respectively. The underlying conditions for successful baryogenesis were formulated by Sakharov \([60]\) and allow for a wide variety of mechanisms, among which leptogenesis \([62]\) is of special interest because it establishes a connection between the Baryon Asymmetry of the Universe (BAU) and the generation of light active neutrino masses.

To explain BAU one must go beyond the SM, either by introducing new sources of CP violation and new kind of out-of-equilibrium situations (through the decay of some new heavy particles), or by modifying the electroweak phase transition itself. In leptogenesis a lepton asymmetry is generated before the electroweak phase transition, which then is converted into BAU in the presence of sphaleron-induced anomalous \(B + L\) violating processes. These convert all primordial lepton asymmetry into a baryon asymmetry. A realization of leptogenesis through the decay of out-of-equilibrium heavy neutrinos transforming as singlets under the SM gauge group was proposed in Fukugita and Yanagida \([62]\). The additional CP violation is provided by the Yukawa couplings through interference between tree and one-loop decay diagrams. The departure from thermal equilibrium occurs when the Yukawa interactions are sufficiently low. The lepton number violation in this scenario is generated from the Majorana masses of the heavy neutrinos, giving rise to lepton number violating decays of the right handed neutrinos:

\[
\begin{align*}
\nu_R &\rightarrow l_i L + \Phi^\dagger \\
\nu_R &\rightarrow l'_i L + \Phi.
\end{align*}
\]

(53)

As usual, CP violation comes from the interference of tree level and one-loop (vertex and self-energy) diagrams. In ALRM, the field entering the heavy neutrino decay is \(H^\dagger\)[\(^\dagger\)]. The CP asymmetry parameter corresponding to the vertex type CP violation is given by

\[
\epsilon^v = \frac{1}{8\pi} \sum_{j=2,3} \text{Im} \left[ \sum_\alpha \frac{\Gamma(\nu_R \rightarrow l_\alpha L + H^+_1) - \Gamma(\nu_R \rightarrow l'_\alpha L + H^-_1)}{\Gamma(\nu_R \rightarrow l_\alpha L + H^+_1) + \Gamma(\nu_R \rightarrow l'_\alpha L + H^-_1)} \right] f_v \left( \frac{m_{N_j}^2}{m_{N_i}^2} \right),
\]

(54)

where \(f_v(x) = \sqrt{x} \left[ 1 - (1 - x) \ln \left( \frac{1+x}{2} \right) \right] \). In addition, CP violation is generated by the interference of the tree level diagram with the one-loop self-energy diagram CP violation, which resembles the CP violation due to the box diagram in \(K^0 - \bar{K}^0\) mixing. If the heavy neutrinos decay in equilibrium, the CP asymmetry arising from the self-energy diagram due to one of the heavy neutrinos may cancel against the asymmetry from the decay of another, to preserve unitarity. However, in out-of-equilibrium decay of heavy neutrinos, the number densities of the two heavy neutrinos differ during their decay, and this cancellation is no longer exact. The CP asymmetry parameter coming from the interference of tree level and one-loop self-energy diagram is given by:

\[
\epsilon^s = \frac{1}{8\pi} \sum_{j=2,3} \text{Im} \left[ \frac{\sum_\alpha \Gamma(\nu_R \rightarrow l_\alpha L + H^+_1 + H^-_1)}{\sum_\alpha \Gamma(\nu_R \rightarrow l_\alpha L + H^+_1 + H^-_1)} \right] f_s \left( \frac{m_{N_j}^2}{m_{N_i}^2} \right),
\]

\(1\)

(55)

\(^1\)The charged components of the bidoublet field also contribute, but their contribution is suppressed by very small Yukawa couplings.
with \( f_s = \sqrt{\frac{2}{\Gamma}} \). In the ALRM scenario considered here, the coupling is \( h_{\alpha i}^* = (Y_{L\alpha}^{i*}) \sin \beta \mathcal{Y}_{N N}^{i*} \) (where we have assumed diagonal Yukawa couplings). These formulas are valid when the neutrino masses are strongly hierarchical \((m_{N_1} \ll m_{N_2}, m_{N_3})\) with \( m_{N_2,3} - m_{N_1} \gg \frac{1}{2} \Gamma_{N_1, N_2,3} \). In such case, the CP-violation arises from the decay of the lightest neutrino, and we have \( \epsilon_s \sim \epsilon_v \). With this, from the required out-of-equilibrium condition, the lower bound on the right-handed neutrino mass is \( m_{N_1} > 10^8 \text{ GeV} \) [63]. However, in our scenario, as discussed in the previous sections, we require \( m_N \) to be in the 1 - 10 TeV range, and thus, this situation does not apply to our case. It has been shown [64] that the mass limits on right-handed neutrinos can be significantly relaxed if two right-handed neutrinos are almost degenerate (resonant leptogenesis) and in this case the masses \( m_{N_1} \sim m_{N_2} \), which can now be in the TeV range. The contribution from the self-energy will now dominate \( (\epsilon_s \gg \epsilon_v) \) with

\[
\epsilon_s^i = \frac{\Im \left[ \sum_{\alpha} (h_{\alpha i}^* h_{\alpha j}) \sum_{\beta} (h_{\beta i}^* h_{\beta j}) \right]}{\left( \sum_{\alpha} |h_{\alpha i}|^2 \right) \left( \sum_{\beta} |h_{\beta j}|^2 \right)} \frac{(m_{N_1}^2 - m_{N_2}^2) m_{N_i} \Gamma_{N_i}}{(m_{N_1}^2 - m_{N_2}^2)^2 + m_{N_1}^2 \Gamma_{N_i}^2},
\]

(56)

where we have

\[
\Gamma_{N_i} = \frac{(h^\dagger h)_{ii}}{8\pi} m_{N_i},
\]

(57)

with the condition,

\[
m_{N_1} - m_{N_2} \approx \frac{1}{2} \Gamma_{N_1, N_2}.
\]

(58)

For the actual values of the masses and widths, this leads to

\[
\frac{(m_{N_1}^2 - m_{N_2}^2) m_{N_i} \Gamma_{N_i}}{(m_{N_1}^2 - m_{N_2}^2)^2 + m_{N_1}^2 \Gamma_{N_i}^2} \approx \frac{1}{2}.
\]

(59)

To achieve baryogenesis by leptogenesis, the baryon asymmetry is related to the CP-violating parameter \( \epsilon \) through the relation \( \Delta B \lesssim 10^{-4} \epsilon_s \), including the washout effects [65]. From eq. (56), this leads to

\[
\frac{3 \left[ \sum_{\alpha} (h_{\alpha i}^* h_{\alpha j}) \sum_{\beta} (h_{\beta i}^* h_{\beta j}) \right]}{\left( \sum_{\alpha} |h_{\alpha i}|^2 \right) \left( \sum_{\beta} |h_{\beta j}|^2 \right)} \approx 10^{-7}.
\]

(60)

to get the required baryon asymmetry as in eq. (62). To investigate further, we need to understand the mixing matrix elements of \( \mathcal{Y}_{N N} \). Recently the T2K experiment has given a 3\( \sigma \) confidence interval for the \( \delta_{CP} \) in the light neutrino sector, which is cyclic and repeats every \( 2\pi \), as \([-3.41, -0.03]\) for the so-called normal mass ordering and \([-2.54, -0.32]\) for the inverted mass ordering [66], but for heavy right-handed neutrinos, we do not have any information.

To choose a simple example, assume only two right-handed neutrinos \( N_1 \) and \( N_2 \), which are quasi-degenerate, contributing maximally to leptogenesis. Then, from the self-energy contribution involving the intermediate \( N_2 \) neutrino, the CP-asymmetry in eq. (56) then gives

\[
|\epsilon_{s N_2}^i| \approx \frac{1}{2} \frac{\Im \left[ (h^\dagger h)_{12} \right]}{(h^\dagger h)_{11} (h^\dagger h)_{22}}.
\]

(61)
For our model

$$
\epsilon^{eN_1}_e \simeq \frac{1}{2} \frac{\Im \left[ \sum \nu^{NN}_0 \nu^{NN}_2 \right]}{\sum_{0} \left| Y^{N_0}_L \right|^2 \left| Y^{N_2}_L \right|^2} \sum_{2} \left| Y^{N_0}_L \right|^2 \left| Y^{N_2}_L \right|^2
$$

\[ = \frac{1}{2} \left( \left| Y^{N_0}_L \right|^2 \left| Y^{N_2}_L \right|^2 \left| Y^{N_1}_L \right|^2 \right) \sum_{2} \left| Y^{N_0}_L \right|^2 \left| Y^{N_2}_L \right|^2 \left| Y^{N_1}_L \right|^2 \left| Y^{N_3}_L \right|^2
\]

(62)

It would be reasonable to assume that all Yukawa couplings are real, and the phases emerging from the right-handed neutrino mixing matrix, for Majorana neutrinos, can be parametrized as

$$
\nu^{NN} = \begin{pmatrix}
C_{12}C_{13}
-S_{12}C_{23}S_{13}e^{i\alpha_{NN}}
-S_{12}C_{23} + S_{12}S_{23}S_{13}e^{i\delta_{NN}}
S_{12}C_{13}
S_{12}S_{23}S_{13}e^{i\delta_{NN}}
S_{23}C_{13}
\end{pmatrix} \text{Diag}(1, e^{i\alpha_{MM}/2}, e^{i\beta_{MM}/2}),
$$

where $S_{ij} = \sin \theta_{ij}^{NN}$, $C_{ij} = \cos \theta_{ij}^{NN}, i, j = 1, 2, 3$, $\delta_{NN}$ is the Dirac phase, and $\alpha_{MM}, \beta_{MM}$ are Majorana phases in the right-handed neutrino mass matrix. Evaluating $\epsilon_{e}$ in terms of the matrix elements

$$
\epsilon_{e}^{eN_1} \simeq \frac{S_{12}C_{23} + C_{12}C_{13}}{S_{12}C_{13} - S_{12}S_{23}S_{13}} (C_{12}S_{23} - C_{13}S_{13}e^{i\delta_{NN}}) \frac{C_{23}}{S_{23}C_{13}} \sin \delta_{NN},
$$

(63)

where we took into account the ordering of Yukawa couplings $Y_{e}^{+} \gg Y_{L}^{+} \gg Y_{e}^{+}$, and approximated $\cos \delta_{NN} \simeq 1$.

Thus, leptogenesis imposes limits on the phases of the mixing matrix for right-handed neutrinos. The expression in eq. (64) depends sensitively on the mixing angles in the matrix. Requiring $|\epsilon_{e}^{eN_1}| < 10^{-6}$, the expression is in general complicated, and we cannot draw any definite conclusions. However, we can estimate the restriction on the Dirac phase in the heavy neutrino mass matrix under some simplifying conditions:

- For $C_{ij}, S_{ij} = \mathcal{O}(10^{-1})$, one would require that the Dirac CP violating phase in the right-handed neutrino mass be, $\sin \delta_{NN} \simeq 10^{-5}$.
- If the matrix is mostly diagonal, $C_{ij} \sim \mathcal{O}(1) \gg S_{kl} \sim \mathcal{O}(10^{-2})$, $\sin \delta_{NN} \simeq 10^{-6}$.
- If the mixing is significant and the mass mixing matrix highly non-diagonal, $S_{ij} \sim \mathcal{O}(1) \gg C_{kl} \sim \mathcal{O}(10^{-2})$, $\sin \delta_{NN} \simeq 10^{-6}$.
- Finally, if the third right-handed neutrino $N_3$ is significantly heavier than the first two and decouples $S_{13} \simeq S_{23} = \mathcal{O}(10^{-2})$, and the first two right-handed neutrinos mix maximally, taking $C_{12} \sim S_{12} \sim 1/\sqrt{2}$, and $(C_{12} - S_{12})^2 \sim \mathcal{O}(10^{-4})$, $\sin \delta_{NN} \simeq 6 \times 10^{-12}$.

These results are promising, because they indicate that, for quite small Dirac phase in the right-handed neutrino mass matrix, the model generates sufficient leptogenesis to satisfy the BAU constraint. Conversely, leptogenesis limits the phase in the right-handed neutrino mass to be quite small. Since in the ALRM the light neutrino masses are generated through flavor breaking, rather than by the seesaw mechanism, this has no direct implication for the Dirac phases in the PMNS matrix.

5 Conclusions

We have explored the ALRM, an alternate way of extending the SM gauge group with a relatively low energy $SU(2)_R$ but without any additional symmetry with the left handed sector, either in gauge couplings
or in the matter content. As has been shown in earlier studies [24] this opens a way to achieve grand unification within $E_6$, while providing a rather unusual model for Dark Matter and an unusual phenomenology also for the vector bosons at the LHC [21]. Indeed, the scotino [25], the partner of the electron in the right-handed doublet in this model can be a viable dark matter candidate and has been studied in several variants of the model [27, 28, 67, 22]. As detailed in Sec. 2, the effective intermediate scale model is $SU(3)_{c} \times SU(2)_{L} \times SU(2)_{R} \times U(1)_{B-L} \times U(1)_{S}$, i.e., the model needs to be enhanced by a global $U(1)_{S}$.

In an earlier attempt to understand the role of $SU(2)_{R}$ extension in $0\nu\beta\beta$ decay, a conventional left-right symmetric model was employed [14], where right-handed charged currents mediated by $W_{R}$ and doubly charged scalars coupling to the leptons, permitting the gauge boson fusion channel, provided interesting new contributions. By contrast here those channels are absent, however the scalar mediated channels become more promising as the relevant Yukawa interactions have new properties. Especially, we find that the induced VEV of the left-handed doublet scalar ($v_{L}$) generates masses for the down-type quarks as well as masses for the light neutrinos, and so it plays a crucial role here. Our study establishes that these new scalar mediated channels contribute significantly to the $0\nu\beta\beta$ in the case of $^{76}$Ge and $^{136}$Xe, the two nuclei experimentally explored. We have found that the contributions to the half-life can be one order larger than the standard $W_{L}$ mediated channels in both the cases, with $T_{1/2}^{WH} \gtrsim 3 \times 10^{26}$ yrs for charged scalar mass of $M_{H^{\pm}} = 200$ GeV, the only parameter that is sensitive to this computation. This is well within the sensitivity expected by future experiments [68, 69].

In addition, the Majorana nature of the neutrinos has the potential to provide the required baryon asymmetry of the universe, through the mechanism of leptogenesis. Studying the resonant leptogenesis, which allows the heavy neutrinos to be in the TeV range, the required CP violation can be easily obtained, even for a small Dirac phase in the right-handed neutrino mass mixing matrix. Thus the ALRM emerging from $E_6$ GUT models provides interesting phenomenological consequences for the Majorana nature of neutrinos and lepton number violation, through enhanced $0\nu\beta\beta$ decay and leptogenesis.

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