Grad-Align+: Empowering Gradual Network Alignment Using Attribute Augmentation

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ABSTRACT

Network alignment (NA) is the task of discovering node correspondences across different networks. Although NA methods have achieved remarkable success in a myriad of scenarios, their satisfactory performance is not without prior anchor link information and/or node attributes, which may not always be available. In this paper, we propose Grad-Align+, a novel NA method using node attribute augmentation that is quite robust to the absence of such additional information. Grad-Align+ is composed of the following key components: 1) augmenting node attributes based on nodes’ centrality measures, 2) calculating an embedding similarity matrix extracted from a graph neural network into which the augmented node attributes are fed, and 3) gradually discovering node pairs by calculating similarities between cross-network nodes with respect to the aligned cross-network neighbor-pair. Experimental results demonstrate that Grad-Align+ exhibits (a) superiority over benchmark NA methods, (b) empirical validation of our theoretical findings, and (c) the effectiveness of our attribute augmentation module.

CCS CONCEPTS
• Computing methodologies → Learning latent representations.

KEYWORDS
Attribute augmentation, centrality, graph neural network, network alignment, node attribute

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1 INTRODUCTION

Network alignment (NA) is the task of discovering node correspondences across different networks. NA is often the very first step in performing downstream machine learning (ML) tasks on multiple networks for more precise analyses [3, 9, 17, 24]. For example, in social networks, the identification of different accounts (e.g., Facebook, Twitter, and Foursquare) of the same user can facilitate cross-site recommendation, friend recommendation, and personalized advertisement [21, 24, 26].

Despite the remarkable success that a number of NA methods [3, 5, 7, 9, 14, 15, 17, 21, 24, 26] are achieving in the NA task, their satisfactory performance is not without supervision data (i.e., prior anchor link information) and/or node attribute information. Nonetheless, such additional information may not always be available in real-world applications [6, 10, 19]; in social networks, cross-network anchor link labeling requires tedious user-account pairing and manual user-background checking, which can be very time-consuming and labor-intensive [19].

Our study is motivated by the observation that the state-of-the-art performance of existing NA methods is significantly deteriorated when prior anchor links and node attributes are unavailable. As illustrated in Figure 1a, NA methods designed by leveraging the prior anchor link information (e.g., PALE [15], FINAL [24], and Grad-Align [21]) tend to reveal high alignment accuracies when prior anchor links are used (albeit slightly); meanwhile, surprisingly, when anchor link information is no longer available, all of them perform very poorly while showing accuracies much lower than 0.1 (see the red circle depicted in Figure 1a). As illustrated in Figure 1b, NA methods making use of underlying node attributes (e.g., GAlign...
We consider source and target networks to be aligned, denoted as $G_s$ and $G_t$, respectively. For $G = (V_s, E_s, X_s)$, the subscript $s$ represents $s$ and $t$ for source and target networks, respectively; $V_s$ is the set of vertices in $G_s$ whose size is $n_s$; $E_s$ is the set of edges in $G_s$; and $X_s$ is the set of original node attributes (i.e., node metadata) in $G_s$, which is optional.

**Definition 2.1.** (NA) Given $G_s = (V_s, E_s, X_s)$ and $G_t = (V_t, E_t, X_t)$, NA aims to find one-to-one node mapping $\pi : V_s \rightarrow V_t$, where $\pi(u) = v$ and $\pi^{-1}(v) = u$ for $u \in V_s$ and $v \in V_t$.

![Grad-Align+ Method](image)

**Figure 2:** The schematic overview of our Grad-Align+ method.

[21], FINAL [24], and Grad-Align [17]) reveal reasonable performance only for attributed networks such as the Douban dataset; thus, their performance drastically degrades for non-attributed network settings with the removal of node attributes.

To tackle this practical challenge, we propose Grad-Align+, a new NA method using node attribute augmentation that is no longer vulnerable to the absence of additional information such as prior anchor links and node attributes. Grad-Align+ is built upon a recent state-of-the-art NA method, named Grad-Align [17], that gradually discovers node pairs by harnessing information enriched through interim discovery of node correspondences during the node matching. Specifically, in the proposed Grad-Align+ method, we first augment node attributes alongside the binning technique based on nodes’ centrality measures. Then, based on the augmented node attributes (and the original node attributes if available), we generate two node representations through two graph neural networks (GNNs) [4], which have emerged as a powerful network feature extractor, trained by using two types of attributes. We then calculate a multi-layer embedding similarity matrix upon the node representations. Finally, we gradually discover node pairs by characterizing a new measure that represents similarities between cross-network nodes with respect to the aligned cross-network neighbor-pair (ACN) [18] to boost the influence of ACNs during the gradual matching. Through comprehensive experiments using real-world and synthetic datasets, we demonstrate that Grad-Align+ (a) enhances the quality of NA, resulting in improving the performance over state-of-the-art NA methods with dramatic gains, (b) empirically validates our theoretical analysis of augmented attributes, and (c) effectively shows the impact and benefits of our attribute augmentation and similarity calculation modules.

## 2 METHODOLOGY

### 2.1 Basic Settings and Problem Definition

We consider source and target networks to be aligned, denoted as $G_s$ and $G_t$, respectively. For $G_s = (V_s, E_s, X_s)$, the subscript $s$ represents $s$ and $t$ for source and target networks, respectively; $V_s$ is the set of vertices in $G_s$ whose size is $n_s$; $E_s$ is the set of edges in $G_s$; and $X_s$ is the set of original node attributes (i.e., node metadata) in $G_s$, which is optional.

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### 2.2 Proposed Grad-Align+ Method

As illustrated in Figure 2, our Grad-Align+ is basically composed of three main components: 1) node attribute augmentation, 2) GNN-based embedding similarity calculation, and 3) gradual NA. We elaborate on each component in the following subsections.

#### 2.2.1 Node Attribute Augmentation

Our node attribute augmentation is built upon the structural consistency assumption that ground truth cross-network node pairs experience the same degree of influence. This motivates us to augment node attributes based on nodes’ centrality measures. In our study, we adopt $k$-hop centrality [16] and Katz centrality [11] among a variety of centrality measures due to their high expressive capability when cross-network node representations are discovered via GNNs using the augmented node attributes.

The $k$-hop centrality is a generalization of degree centrality and measures the influence of all nodes within $k$ hops from the node of interest while the contributions of distant nodes are penalized. The $k$-hop centrality of node $i$ in $G_s$ is formulated as $c_{i,s} = \sum_{l=1}^{k} \frac{n_{l,s}(i)}{\alpha_l}$, where $n_{l,s}(i)$ is the number of nodes whose path length from node $i$ is at most $l$ and $\alpha$ is a penalizing constant. On the other hand, the Katz centrality can be viewed as a variant of eigenvector centrality [1] and measures the influence of a node on its higher-order neighbors at larger distances while penalizing higher-order connections. The Katz centrality of node $i$ in $G_s$ is defined as $c_{i,s} = \alpha \sum_{j \in V_s} a_{ij} c_{j,s} + \beta$, where $a_{ij} = (i,j)$-th element of the adjacency matrix of $G_s$, and $\alpha$ and $\beta$ are constants. Note that $k$-hop centrality is calculated in a localized manner while Katz centrality captures both the local and global influences of a node.

To create node attribute vectors, we discretize the above centrality measures with a fixed dimension $d$. To this end, we employ the equal-width binning technique [2]. Precisely, for node $i$ in $G_s$, we generate the $d$-dimensional one-hot encoded attribute vector, denoted as $\tilde{x}_{i,s}$ corresponding to the $i$-th element of matrix $X_s$, in such a way that $i$ is assigned to the $\left\lfloor \frac{w_{i,s}}{w} \right\rfloor$-th element of $\tilde{x}_{i,s}$, where $w$ is the binning width. A higher $w$ leads to a lower $d$ due to the fact that $d = \left\lfloor \frac{c_{\text{max,s}}}{w} \right\rfloor$, where $c_{\text{max,s}}$ is the maximum centrality among nodes in $G_s$. To avoid a small number of influential nodes to increase the vector dimension, we remove the vector components whose value is never assigned over the two networks. We shall examine how the selection of $d$ affects the performance of Grad-Align+ in Section 3.2.

#### 2.2.2 GNN-based Embedding Similarity Calculation

We describe how to calculate the multi-layer embedding similarity matrix via GNNs using augmented node attribute vectors. We start by stating the augmented node attributes and original node attributes are often heterogeneous since our augmentation strategy is designed based on the structural information. In this context, instead of naively concatenating two types of attribute vectors, we use two different GNN models, $GNN_{\theta_1}$ and $GNN_{\theta_2}$, into which two attributes are fed separately (see Figure 2). The model parameters $\theta_1$ and $\theta_2$ are trained by a layer-wise reconstruction loss in [17] to make each node representation more distinguishable. Using the hidden representations $H_s(1) \in \mathbb{R}^{n_s \times h}$ and $H_t(1) \in \mathbb{R}^{n_t \times h}$ at each layer extracted from $GNN_{\theta_1}$ and $GNN_{\theta_2}$, respectively, for the dimension
where $\lambda$ is a hyperparameter balancing two terms in Eq. (1). For networks without node metadata, we only use the second term.

Next, we analyze how augmented attributed vectors influence the resulting vector representations via GNNs. Let $\hat{h}_{u,t}$ and $\hat{h}_{v,t}$ denote hidden vector representations of nodes $u \in \mathcal{V}_t$ and $v \in \mathcal{V}_t$, respectively. Then, for a ground truth node pair $(u,v)$, it is highly probable to have a small $\|\hat{h}_{u,t} - \hat{h}_{v,t}\|_2$ in the embedding space, where $\|\cdot\|_2$ is the $L_2$-norm of a vector (or a matrix). For ease of analysis, for ground truth node pairs, we make the following two assumptions: 1) $\mathbb{E}[\|\hat{x}_{u,t} - \hat{x}_{u,t}\|_2]$ is arbitrarily small, that is, augmented attributes are consistent, and 2) all the neighbors of $(u,v)$ are ACNs.\(^1\) Now, we are ready for establishing the following theorem.

**Theorem 2.2.** Consider the pre-activation output of the 1-layer GCN model in which the weight matrix $W$ is shared. Suppose that $\mathbb{E}[\|\hat{x}_{u,t} - \hat{x}_{u,t}\|_2] \leq \epsilon$ for an arbitrarily small $\epsilon > 0$ by the attribute consistency assumption. Then, given a ground truth node pair $(u,v)$ for $u \in \mathcal{V}_t$ and $v \in \mathcal{V}_t$, $\mathbb{E}[\|\hat{h}_{u,t} - \hat{h}_{v,t}\|_2]$ is bounded by $\|W\|_2\epsilon$.

2.2.3 Gradual NA. We explain how to gradually match node pairs using a similarity matrix in each gradual step. In this phase, the selection of a similarity measure plays a significant role in determining the performance of NA. In our study, rather than adopting prior approaches based on the Jaccard index [5] and the Tversky similarity [18, 22], as another main contribution, we present our new measure that represents similarities between cross-network nodes, the so-called ACN similarity, which is formulated as:

$$S_{ACN}^{(i)}(u,v) = ACN_{u,v}^P,$$

where $S_{ACN}^{(i)}(u,v)$ is the $p$-th power of the number of ACNs between node pair $(u,v)$ for $u \in \mathcal{V}_t$ and $v \in \mathcal{V}_t$ at the $i$-th iteration, corresponding to the $(u,v)$-th element of matrix $S_{ACN}^{(i)}$. Finally, following the dual-perception similarity in Grad-Align, we calculate the similarity matrix $S^{(i)}$ as follows:

$$S^{(i)} = S_{emb} \odot S_{ACN}^{(i)},$$

where $\odot$ indicates the element-wise matrix multiplication operator. The rest of the gradual node matching essentially follows that of [18].

3 EXPERIMENTAL EVALUATION

3.1 Experimental Setup

Datasets. We conduct experiments on five benchmark datasets consisting of three real-world datasets, including Facebook vs. Twitter (Fb-Tw) [1], Douban Online vs. Douban Offline (Do-Doff) [25], and Allmovie vs. IMDb (Am-ID), and two synthetic datasets, including Facebook and Econ [20]. For synthetic datasets, we generate a noisy version of the original network by randomly removing 10% of edges and flipping 10% of binary-valued node attributes.

\(^1\)The second assumption is sensible since ground truth node pairs tend to share lots of ACNs in real-world applications [3].

### Table 1: Empirical analysis on node attributes, node representations, and accuracies according to different centrality measures on Facebook.

| Centrality | $\mathbb{E}[\|\hat{x}_{u,t} - \hat{x}_{u,t}\|_2]$ | $\mathbb{E}[\|\hat{h}_{u,t} - \hat{h}_{u,t}\|_2]$ | Acc |
|------------|---------------------------------|---------------------------------|-----|
| 1-hop      | 0.33                            | 5.21                            | 84.08 |
| 2-hop      | 0.64                            | 5.57                            | 50.91 |
| 3-hop      | 0.61                            | 5.51                            | 72.58 |
| Katz       | 0.50                            | 5.01                            | 83.22 |

**Performance metrics.** As the most popular metrics, we adopt the alignment accuracy, denoted as Acc, and Precision@q (also known as Success@q) as in [5, 18, 24].

**Competitors.** We compare Grad-Align+ with 5 state-of-the-art NA methods, which are divided into two different categories: NA methods that necessitate supervision data (i.e., prior anchor links) (FINAL [24] and PALE [15]) and NA methods that can be carried out without supervision data (Grad-Align [17], CENALP [5], and GALign [21]).

**Implementation details.** We first describe experimental settings of GNNs. We use GIN [23] as it is validated to exhibit the best performance among well-known GNN models such as GCN [13] and GraphSAGE [8] (see [18] for more details). We train our GNN model using Adam optimizer [12] with a learning rate of 0.005. For the binning technique, we use 1-hop centralities for the Fb-Tw, Facebook, and Econ datasets and Katz centrality for other datasets unless otherwise stated. For Grad-Align and GALign, following their original settings, we use all-ones vectors $1 \in \mathbb{R}^{1\times n_u}$ and $1 \in \mathbb{R}^{1\times n_v}$ as the input of node attributes. We basically assume unsupervised settings where prior anchor links are unavailable. Nevertheless, for the NA methods that should operate on supervision data, we use randomly selected 5% of prior anchor links as supervision data although our method is handicapped accordingly.

3.2 Experimental Results

Our extensive empirical studies are designed to answer the following four key research questions (RQs).

- **RQ1:** How does the choice of centrality in attribute augmentation affect the model performance?
- **RQ2:** How do key parameters affect the performance of Grad-Align+?
- **RQ3:** How much does Grad-Align+ improve the NA performance over state-of-the-art NA methods?
- **RQ4:** How much is our attribute augmentation module beneficial to the performance boost of NA methods?

(RQ1) Impact of attribute augmentation. We empirically show how node representations behave according to different nodes’ centrality measures used for attribute augmentation. To purely examine the impact of augmentation without the original node attributes, we use the Facebook dataset belonging to non-attributed networks in this experiment. From Table 1, it is likely that, given ground truth node pairs $(u,v)$ for $u \in \mathcal{V}_t$ and $v \in \mathcal{V}_t$, a lower $\mathbb{E}[\|\hat{x}_{u,t} - \hat{x}_{u,t}\|_2]$ leads to a lower $\mathbb{E}[\|\hat{h}_{u,t} - \hat{h}_{u,t}\|_2]$, thereby resulting in a higher alignment accuracy. This is consistent with Theorem 2.2 in the sense that $\mathbb{E}[\|\hat{x}_{u,t} - \hat{x}_{u,t}\|_2]$ is bounded by $\mathbb{E}[\|\hat{x}_{u,t} - \hat{x}_{u,t}\|_2]$ to within a constant factor.

(RQ2) Effect of key parameters. In Figure 3, we investigate the effect of parameters used in Grad-Align+ and experimental settings, including the dimension of augmented attribute vectors, $d$, the
Table 2: Performance comparison among Grad-Align+, and 5 state-of-the-art NA methods in terms of the Acc and Precision@q. Here, the best and second-best performers are highlighted by bold and underline, respectively.

| Method               | Metric | Fb-Tw | Do-Doff | Ad-ID | Facebook | Econ | Unsup. |
|----------------------|--------|-------|---------|-------|----------|------|--------|
| PALE                 | Acc    | 0.5923 | 0.3052 | 0.3232 | 0.6077  | 0.5819 |
|                      | Precision@5 | 0.6051 | 0.1783 | 0.6244 | 0.6040  | 0.6041 |
|                      | Precision@10 | 0.7030 | 0.2338 | 0.7519 | 0.7162  | 0.6836 |
| FINAL                | Acc    | 0.6328 | 0.2773 | 0.6125 | 0.5780  | 0.4185 |
|                      | Precision@5 | 0.6475 | 0.4358 | 0.7592 | 0.5509  | 0.4467 |
|                      | Precision@10 | 0.7253 | 0.5824 | 0.8152 | 0.7158  | 0.5841 |
| CENALP               | Acc    | 0.9105 | 0.0251 | 0.4238 | 0.4237  | 0.4972 |
|                      | Precision@5 | 0.9370 | 0.0571 | 0.7211 | 0.6278  | 0.5328 |
|                      | Precision@10 | 0.9405 | 0.1130 | 0.7154 | 0.7115  | 0.6271 |

The effect of $d$: Note that the node attributes are augmented based on nodes’ centrality (i.e., structural information). Thus, it is possible to further enhance the expressiveness of networks having strong structural consistency by increasing the value of $d$. As shown in Figure 3a, the performance tends to monotonically increase with $d$ on Fb-Tw while it is rather degraded beyond a certain value of $d$ on Do-Doff due to the excessive use of structural information in networks revealing structural inconsistency.

The effect of $p$: The results from Figure 3b essentially show a tendency similar to those in Figure 3a. The overexploitation of ACNs during the node matching on Do-Doff exhibiting strong structural inconsistency turns out to degrade the performance.

The effect of $t$: From Figure 3c, it is obvious that the Acc monotonically increases with more supervision data. One can see that Grad-Align+ still guarantees quite reasonable performance even in unsupervised settings (i.e., $t = 0$) unlike existing NA methods (refer to Figure 1).

(RQ3) Comparison with five competitors. Table 2 presents the performance comparison between Grad-Align+ and 5 state-of-the-art NA methods with respect to the Acc and Precision@q for $q \in \{5, 10\}$ using three real-world and two synthetic datasets. Here, Unsup. represents the methods that are run unsupervisedly without any prior anchor links. Grad-Align+ consistently and significantly outperforms all the competitors regardless of the datasets and the performance metrics while showing gains up to 47.03% compared to the second-best performer. However, the second-best performer depends on the datasets, which implies that one does not dominate other competitors. More interestingly, existing GNN-based NA methods (i.e., Grad-Align and GAlign) perform poorly on the datasets without node attributes such as Fb-Tw and Facebook. This indicates that the augmented node attributes play a crucial role in generating precise representations of each node, thus resulting in a substantial performance improvement.

(RQ4) Impact of our attribute augmentation module. Our node attribute augmentation module can also be integrated into other NA methods that leverage attribute information. To investigate the impact of attribute augmentation in such NA methods, we conduct an ablation study by removing this module and summarize the evaluation results in terms of the Acc using the Facebook dataset in Table 3. Dramatic gains over the cases without attribute augmentation are achieved when Grad-Align and Grad-Align+ are employed. Since the accuracy of interim discovery of node correspondences is critical in gradually discovering node pairs, attribute augmentation can most benefit both Grad-Align and Grad-Align+ by helping discover correct node pairs, especially in the early stage of gradual node matching.

4 CONCLUDING REMARKS

In this paper, we aimed to devise a methodology that substantially improves the performance of NA in unsupervised settings. Toward this goal, we proposed Grad-Align+, the high-quality NA method that judiciously integrates the GNN model trained along with augmented node attributes based on $k$-hop and Katz centrality measures into the gradual node matching framework. Through extensive experiments, we demonstrated the effectiveness of our augmentation module with its theoretical validity as well as the superiority of Grad-Align+ over the state-of-the-art NA method with gains of up to 47.03%.

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