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We demonstrate experimentally that a sizable chiral charge pumping can be achieved at room temperature in graphene/Yttrium Iron Garnet (YIG) bilayer systems. The effect, which cannot be attributed to the ordinary spin pumping, reveals itself in the creation of a dc electric field/voltage in graphene as a response to the dynamic magnetic excitations (spin waves) in an adjacent out-of-plane magnetized YIG film. We show that the induced voltage changes its sign when the orientation of the static magnetization is reversed, clearly indicating the broken mirror reflection symmetry about the planes normal to the graphene/YIG interface. The strength of effect shows a non-monotonous dependence on the spin-wave frequency, in agreement with the proposed theoretical model.

I. INTRODUCTION

The generation of spin-polarized currents is of technological interest in order to transmit information encoded in the spin degrees of freedom. A spin current can be injected into a nonmagnetic conductor by spin pumping.1,2 In this process, the reservoir of the angular momentum is a ferromagnet where a ferromagnetic resonance (FMR) is excited by a microwave field. The spin pumping without net charge transport stems from the exchange of angular momentum between the itinerant spins in the metal and the collective magnetization dynamics in the adjacent ferromagnet. The dynamical generation of spin currents is of special relevance since alternative methods based on driving an electrical current through the interface are limited by the conductance mismatch.3 The spin pumping-induced currents have been detected as the long-ranged dynamic interaction between two ferromagnets separated by a normal metal4,5 or as a dc-voltage signal in bilayer systems.6 In the case of nonmagnetic metals with a strong spin-orbit coupling, the spin current through the interface may engender a charge current along the metallic layer as result of the inverse spin-Hall effect.7,8 As the thickness of the metallic layer is reduced, additional interfacial effects must be considered. The different contributions may be identified by analyzing the symmetries of the voltage signal with respect to different adjustable parameters, such as the orientation of the saturated magnetization controlled by the applied static field.9 Additionally, we can use propagating spin waves instead of FMR and vary the direction of propagation.

Among other materials, the unique candidate for investigations of interface-induced phenomena is single layer graphene (SLG). Due to its unique mechanical, optical, and electronic properties, graphene has attracted enormous attention since its discovery in 2004.10,11 Nowadays, one can produce large-area high-quality SLG by using, e.g., chemical vapor deposition on metal catalysts.12–14 For the observation of spin pumping effects, SLG should be brought in contact with a magnetic material. Yttrium Iron Garnet (YIG) holds a special place among all magnetic materials. Specifically, it shows an unprecedentedly small magnetic damping resulting in the narrowest known line of the FMR and enabling propagation of spin waves over long distances.15,16 Due to these unique characteristics, YIG films have been recently considered as a promising material for spintronic and magnonic applications.17,18 By combining YIG and SLG in a bilayer, one obtains a unique model system for investigations of the spin-wave induced interfacial effects.

Here, we report the observation of a chiral charge pumping in out-of-plane magnetized YIG/SLG bilayers, depicted in Fig. 1 a). We show that spin waves propagating in the YIG film induce a sizable electric voltage in the adjacent SLG due to a proximity exchange coupling.19 We study the symmetry of the observed phenomenon by reversing the out-of-plane static magnetic field and the direction of spin-wave propagation. The change in the sign of the electric voltage under the inversion of the magnetic field indicates a broken mirror reflection symmetry about the plane normal to the interface (of the nature of the symmetry breaking between clockwise and counterclockwise rotations in the plane), confirming the chiral nature of the effect. We would like to emphasize that the conventional spin pumping-induced voltages obtained for in-plane magnetized films20–22 are rooted in the reflection symmetry breaking about the plane of the interface. The dc-voltage reported here is along the direction of propagation of spin waves, and therefore it is unrelated to the spin Hall phenomenology.

The suggested structural chirality of the device, however, may not be evident from the nominal material growth and the deposited contact configuration, which are expected to respect this symmetry. A structural chirality may, however, be endowed during the epitaxial growth or polishing procedure, when involving substrate rotation. One possibility for this chirality to man-
manifest in our structure is through a chiral imbalance of screw dislocations in the crystalline lattice of YIG. We present a theoretical model, which shows that such crystalline defects effectively tilt the exchange field experienced by majority carriers in SLG, resulting in a charge pumping with the observed symmetry. Moreover, in agreement with the experiment, our model predicts a non-monotonic dependence of the induced voltage on the spin-wave frequency.

The structure of the manuscript is the following: We present the microwave and voltage measurements in Sec. II. Special attention is paid to the inversion symmetry breaking, confirmed by further FMR experiments in YIG, revealing the chiral nature of the effect. The theoretical model is discussed in Sec. III. Technical details of the model are set-aside in the Appendix. We summarize our findings in Sec. IV.

II. EXPERIMENT

A. Preparation and characterization of the YIG/SLG bilayer

The experimental layout for studies of the voltage induced by spin waves in YIG/SLG bilayer is shown in Fig. 1 a). Graphene was placed on top of a monocrystalline YIG film of 5.1 µm thickness grown by means of liquid phase epitaxy on 0.5 mm thick gallium gadolinium garnet (GGG) substrate. The saturation magnetization of the YIG film defining the saturation field in the out-of-plane geometry was $4\pi M_S = 1.75$ kG. The SLG sample was grown on a 50 µm thick 99.99% pure copper foils in a cold-wall low-pressure CVD reactor (Black Magic, AIXTRON). After the Cu foil had been cleaned in acetone and then shortly etched in acetic acid to remove surface oxide, it was placed on a graphitic heater inside the reactor and annealed at 1000 °C during 5 min in a flow of 20 sccm H$_2$ and 1000 sccm Ar. Then, a flow of pre-diluted CH$_4$ (5% in Ar, 30 sccm) was introduced during 5 min to initiate the growth of graphene. After the growth, the gas flow was shut down, the system evacuated to < 0.1 mbar and cooled down to room temperature. SLG was transferred to YIG/GGG by using the bubbling delamination technique and lithographically patterned into a multi-terminal Hall-bar structure with Au(100 nm)/Cr(5 nm) pads at the edges. The lateral dimensions of the sample were 1.5 by 25 mm. The Hall-effect mobility of the resulting devices was found to be in the range from 600 to 1300 cm$^2$ (V·s)$^{-1}$ at $T = 10$ K. The local resistance maximum at zero magnetic field $H_0 \approx 0$, usually ascribed to the weak localization effect, allowed for an estimation of the phase coherence length $L_\phi \sim 100$ nm at the same temperature.

B. Microwave and voltage measurements

The YIG/SLG sample was built onto a massive metal holder whose temperature was controlled and kept constant at 295 ± 0.02 K. The holder with the sample was placed between the poles of an electromagnet, which cre-
FIG. 2: Symmetry properties of the observed effect. Both the induced electric field $E$ and the wavevector of the spin wave $k_{sw}$ defining the direction of spin-waves propagation are in the plane of the sample, while the applied field $H_0$ and the YIG-magnetization $M_S$ are oriented normally to the sample plane. The $+$ and $-$ signs indicate the polarity of the measured dc-voltage. a) The reference geometry. b) Rotation of the system by $180^\circ$ around the $z$-axis reverses the directions of both $E$ and $k_{sw}$. In agreement with experiment, the sign of the voltage is reversed. c) Mirroring with respect to the vertical $xz$-plane ($y \rightarrow -y$) does not change vectors $E$ and $k_{sw}$, while axial vectors $H_0$ and $M_S$ are reversed. In contrast to the experimental findings, the sign of the voltage is not reversed.

Simultaneously with the microwave measurements, we recorded the dc-voltage between the electrodes. A lock-in technique was applied in order to detect the dc-voltage caused by the spin waves propagating in the YIG film. Microwaves were modulated by a square wave with the repetition frequency of 10 kHz and the voltage difference between different leads was measured by the lock-in amplifier. During the measurements, the orientation of the out-of-plane static magnetic field was reversed and the dc-voltage along with the reflected MW power signal as a function of $H_0$ was recorded. It is important to note that the dc-voltages measured on both sides of SLG (as depicted in Fig. 1 a) were the same within experimental errors. Thus, the existence of a circular induced electric field can be excluded. Fig. 1 c) shows a typical dependence of the measured voltage versus the applied magnetic field. Comparing Figs. 1 b) and c), one sees that the dc-voltage in SLG is induced at the same values of $H_0$, where the efficient excitation of spin waves takes place. This clearly indicates its direct connection to the high-frequency magnetization precession in YIG.

C. Symmetry breaking

The most striking feature of the observed phenomenon is its unusual symmetry with respect to the inversion of $H_0$. As seen from Fig. 1 c), the detected voltage changes its sign if the orientation of $H_0$ (and $M_S$) is reversed. We emphasize that this inversion is not accompanied by visible changes in the microwave absorption curve (Fig. 1 b). Further measurements show that the induced voltage is proportional to the intensity of the spin wave (the absorbed microwave power) and changes sign if the direction of the spin-wave propagation is reversed.
To obtain better insight into the underlying physics, we consider the symmetry of the phenomenon in more detail. As shown in Fig. 2, the induced electric field \( E \) is oriented in the sample plane parallel to the direction of the spin-wave propagation indicated in Fig. 2 by a vector \( k_{sw} \), whereas the magnetization/magnetic field is perpendicular to the sample plane. The + and − signs indicate the polarity of the measured dc-voltage at a given orientation of the magnetization. As seen in Fig. 2 b), rotation by 180° around the normal to the film plane reverses both the direction of the spin-wave propagation and that of the electric field, whereas the direction of the magnetization stays unchanged, all in agreement with the experimental findings. Before discussing the situation depicted in Fig. 2 c), which is obtained from that of Fig. 2 a) by mirroring of the system with respect to the vertical \( xz \)-plane \((y \rightarrow −y)\), one should realize that all the vectors \( E \), \( k_{sw} \), \( H_0 \) and \( M_S \) are in the \( xz \)-plane. However, real and axial vectors have different properties with respect to mirroring. Correspondingly, since \( E \) and \( k_{sw} \) are real vectors, the above mirroring does not inverse them. As a consequence, the sign of the measured dc-voltage should not be changed. In contrast, \( H_0 \) and \( M_S \), which are axial vectors, are reversed by the mirroring.

We emphasize that this contradicts to the experiment that shows a change in the voltage sign by inversion of the applied field. We come to the same conclusion when the system is mirrored about the \( yz \)-plane \((x \rightarrow −x)\). In other words, the phenomenon responsible for the appearance of the voltage in the YIG/SLG bilayer requires that the mirror reflection symmetry about the planes normal to the interface is broken. More specifically, the observed effect would be forbidden if the clockwise and counter-clockwise directions in the sample plane were equivalent, which reveals its chiral nature.

D. FMR measurements

To check whether the observed non-equivalence is a characteristic feature of the YIG film itself, we performed high-precision FMR measurements on YIG films of small lateral dimensions (5.1 \( \mu \)m thick circle with the 0.5 mm radius and 6 \( \mu \)m thick 0.5 \( \times \) 0.5 mm\(^2\) square) without SLG. In these experiments, the FMR in the YIG sample was excited by a quasi-uniform dynamic magnetic field. The entire test device was mounted on a non-magnetic rotatable sample holder (see the inset in Fig. 3 a), which was placed in a static magnetic field with a homogeneity better than 0.1 Oe, with the \( x \)-axis being the rotation axis of the holder. Note here that the actual rotation axis (the \( x \)-axis) in the described experiments differs from the rotation axis of the thought experiment (the \( z \)-axis) shown in Fig. 2. The sample holder was designed to keep the position of the sample constant with an accuracy of 0.2 mm over the entire rotation. By sweeping the microwave frequency at a fixed magnetic field, the transmission coefficient \( T = P_{out}/P_{in} \) was measured as a function of the frequency. Then, the holder with the sample was rotated by 180°, and the measurements were repeated. The results of the measurements for the two orientations of the sample were averaged over several measurement cycles. The obtained FMR curves for the up \((H_+)\) and down \((H_-)\) orientations of the static field demonstrating a clear frequency difference of \( \Delta f = 5 \) MHz are shown in Fig. 3 a). The value of \( \Delta f \) is significantly larger compared to the estimated uncertainty of 0.5 MHz originating from the inhomogeneity of the static field and the stray fields of the sample holder. The measurements were repeated for different values of the applied magnetic field resulting in the field dependence of \( \Delta f \) shown in Fig. 3 b).

One clearly sees that \( \Delta f \) systematically increases as \( H_0 \) approaches \( 4\pi M_S = 1.75 \) kG. Qualitatively similar results were obtained for different samples except that the maximum values \( \Delta f \) were found to vary from 6 to 13 MHz.

The results presented in Fig. 3 show that the frequency of the FMR in YIG films depends on whether the static magnetic field is parallel or antiparallel to the normal to the film surface \( \hat{z} \), i.e. it depends on the direction (clockwise or counter-clockwise with respect to \( \hat{z} \)) of the magnetization precession. This indicates that the mirror reflection symmetry about the planes normal to the YIG/SLG interface is broken, since the clockwise and the counter-clockwise directions in the plane of the film are not equivalent. Although the microscopic origin of this breaking is not yet fully clear, it should be connected with the defects in the crystallographic structure of YIG, since the ideal high-symmetry cubic structure of YIG is definitely incompatible with this symmetry breaking. It is known that the dominating defects in high-quality epitaxial YIG films are growth dislocations. Their typical lateral density of about \( 10^8 \) cm\(^{-2}\) is connected with the typical misfit between YIG and GGG lattices of \( 10^{-3} \) (see Refs. 15,27). It is also known that such dislocations strongly influence the magnetic dynamics in YIG.28 Possible mechanisms of the defect-mediated
symmetry breaking can include a growth-induced imbalance between clockwise and counter-clockwise screw dislocations in conjunction with a spin-orbit interaction.\textsuperscript{29}

We emphasize that, although the symmetry breaking is present in YIG films without SLG on top, its influence on the magnetization dynamics is very small and can only be detected in high-precision measurements. This is not surprising, since the symmetry breaking appears to be a surface phenomenon, which has vanishing influence on the magnetization in the bulk of the film. On the contrary, this symmetry breaking is expected to have significant influence on conduction electrons in SLG placed on the surface of the YIG film.

III. PHENOMENOLOGICAL MODEL

Next, we provide a phenomenological model for the observed effect based on the existence of a finite density of screw dislocations in YIG. The voltage signal is related with the electromotive forces induced by the magnetization dynamics. A screw dislocation creates a distortion of the graphene lattice as shown in Fig. 4 a), which couples to the electron spin through the spin-orbit interaction. As a result, the exchange field seen by the itinerant electrons is tilted with respect to the magnetization in YIG, Fig. 4 b), modifying the longitudinal response in the non-adiabatic regime. We emphasize that this mechanism must be taken as a suggestive explanation for the observed phenomenon since there is no direct observation of the proposed mechanical deformations.

A. Hamiltonian

We assume that the exchange interaction couples the spins of itinerant electrons of SLG to the localized magnetic moments in YIG. The Hamiltonian reads as

\begin{equation}
\mathcal{H} = \hbar v_F \Sigma \cdot p + \Delta_{\text{ex}} \mathbf{m}(t,r) \cdot \mathbf{s} + \mathcal{H}_{\text{so}},
\end{equation}

The first term is the Dirac Hamiltonian describing electronic states with momentum \( p \) around the two inequivalent valleys \( K_{\pm} \) in graphene, where \( \Sigma = (\pm \sigma_x, \sigma_y) \) is a vector of Pauli matrices associated to the sub-lattice degree of freedom of the wave function and \( v_F \) is the Fermi velocity. The second term corresponds to the exchange coupling, \( \Delta_{\text{ex}} \), where \( \mathbf{s} = (s_x, s_y, s_z) \) are the itinerant spin operators and \( \mathbf{m}(t,r) \) is a unit vector along the local magnetization in YIG. The last term is a spin-lattice interaction that couples the mechanical degrees of freedom with the spins of electrons.

As it is well known,\textsuperscript{11} graphene can support large mechanical distortions that change dramatically the dynamics of Dirac electrons. When an SLG is placed on top of disturbed YIG, the carbon atoms near a screw dislocation can be expected to follow its distorted profile, which introduces a torsion in the honeycomb lattice, as represented in Fig. 4 a). This deformation couples to the electron spin as

\begin{equation}
\mathcal{H}_{\text{so}} = \Delta_{\text{so}}(\partial_x u_y - \partial_y u_x)(\sigma_x s_x + \sigma_y s_y),
\end{equation}

where \( \partial_x u_y - \partial_y u_x \) is the anti-symmetrized strain tensor and \( u = (u_x, u_y) \) represents the displacements of the carbon atoms – that parameterizes the torsion of the graphene lattice and can on average be related to the density of screw dislocations. The form of this coupling is dictated by the \( C_{6v} \) symmetry of the honeycomb lattice, and its microscopic origin resides in the hybridization of \( \pi \) and \( \sigma \) orbitals of carbon atoms, which enhances the spin-orbit effects within the low-energy bands.\textsuperscript{30} This is the minimal spin-lattice Hamiltonian that incorporates both the out-of-plane \( (z \rightarrow -z) \) and in-plane mirror symmetry breaking present in our sample. The proposed deformation in Fig. 4 just models the observed symmetry breaking to provide a proof of principle for the chiral charge pumping. We expect our model to be qualitatively correct regardless of the actual deformations of the lattice close to dislocations.

The effective exchange field seen by itinerant electrons, \( \mathbf{n}(t,r) \), is tilted away from the local magnetization following the torsion of the lattice, as illustrated in Fig. 4 b). This is implemented by the spin-lattice coupling in Eq. (2), which can be understood on geometry grounds as the non-abelian connection that transports the spin quantization axis along the distorted graphene lattice. The details are provided in the Appendix. To the lowest order in \( \Delta_{\text{so}} \), we obtain

\begin{equation}
\mathbf{n}(t,r) \approx \mathbf{m}(t,r) - \frac{2\Delta_{\text{so}}}{\hbar v_F} \mathbf{b}(r) \times \mathbf{m}(t,r),
\end{equation}

where \( \mathbf{b}(r) \) is defined as

\begin{equation}
\mathbf{b}(r) = a^{-1} \int_{r_0}^{r} dr' (\partial_x u_y - \partial_y u_x).
\end{equation}
Here \( r_0 \) is the origin of the dislocation and we have introduced a microscopic length scale \( a \) in order to make \( b(\mathbf{r}) \) dimensionless.

### B. Electromotive forces

The magnetization dynamics induces electromotive forces in SLG along the direction of propagation of spin waves. At low frequencies, majority electrons along the quantization axis defined by \( \mathbf{n}(t, \mathbf{r}) \) experience an effective electric field of the form \( E_i = \frac{\hbar}{2e} \hat{n} \cdot (\mathbf{n} \times \partial_t \mathbf{n} + \beta \partial_i \mathbf{n}) \).

\[
E_i = \frac{\hbar}{2e} \hat{n} \cdot (\mathbf{n} \times \partial_t \mathbf{n} + \beta \partial_i \mathbf{n}). 
\]

The first term is purely geometrical, strictly valid in the limit \( \Delta_{\text{ex}} \gg \hbar |\hat{n}|, \hbar v_F |\partial_t \mathbf{n}| \), when the electron spins follow adiabatically the direction of effective exchange field. The \( \beta \) correction is related to a slight misalignment due to spin relaxation caused by the spin-orbit interaction.

The electromotive force in the adiabatic limit, which is rooted in the associated geometrical Berry phase, respects the structural symmetries of the device. Indeed, the correction due to the magnetization tilting expressed in Eq. (3) averages to 0 when integrated upon the period of the spin wave excitation. The introduction of screw dislocations in YIG breaks the structural symmetries of the transport signals in SLG owing only to non-adiabatic corrections to the electromotive force. These appear as higher order expansions in \( \frac{1}{\Delta_{\text{ex}}} \mathbf{n} \) and spatial gradients \( \frac{\hbar v_F}{\Delta_{\text{ex}}} \partial_t \mathbf{n} \) that capture spin-orbital effects. The new terms compatible with \( C_{6v} \) symmetry read

\[
E_i = \frac{\hbar^3 v_F}{2e \Delta_{\text{ex}}^2} (\beta_1 \partial_i \mathbf{n} + \beta_2 \mathbf{n} \times \partial_i \mathbf{n}) \cdot \hat{z} \times \nabla (\hat{n})^2 , \tag{6}
\]

where \( \beta_1,2 \) are dimensionless phenomenological parameters. The tilting of the exchange field translates the effect of the symmetry breaking in YIG into the electronic response of graphene, driving a voltage along the direction of propagation of the spin waves of the form

\[
V = \frac{\beta_1 \hbar^2 v_F}{\Delta_{\text{ex}}^2} \int dx (\partial_y u_y - \partial_y u_x) \hat{z} \cdot \mathbf{m} \partial_x (\hat{m})^2 . \tag{7}
\]

As seen from this equation, the proposed theoretical model reproduces the experimentally observed inversion of the sign of the induced voltage accompanying the reversal of the magnetization \( (\hat{z} \cdot \mathbf{m} \rightarrow -\hat{z} \cdot \mathbf{m}) \) when \( H_0 \rightarrow -H_0 \) or the direction of the spin-wave propagation \( (\partial_x (\hat{m})^2 \rightarrow -\partial_x (\hat{m})^2 \) when \( k_{\text{sw}} \rightarrow -k_{\text{sw}} \)).

The contribution in Eq. (7) should saturate when the theory crosses over to the strongly non-adiabatic regime, at frequencies of the order of \( \Delta_{\text{ex}}/\hbar \). We expect for the electromotive force to be suppressed at larger frequencies due to a dynamic averaging effect, similarly to the motional narrowing in the spin diffusion problem: the magnetization precession is so fast that its time-dependent component effectively averages out from the view of electron spins.

### C. Frequency dependence

The model predicts that the effect should exist only within a certain range of spin-wave frequencies around \( \Delta_{\text{ex}}/\hbar \). Although \( \Delta_{\text{ex}} \) cannot be directly measured in the experiment, the theoretical prediction can be verified by analyzing the frequency dependence of the observed effect. Figure 5 a) shows the measured voltage, averaged over the field interval where spin waves are efficiently excited at a given frequency (cf. Figs. 1 b and 1 c) versus the absorbed microwave power, \( P_{\text{abs}} \) proportional to the intensity of the excited spin waves. As seen from Fig. 5 a), the voltage is linearly proportional to the spin-wave intensity and the proportionality coefficient \( V/P_{\text{abs}} \) is indeed strongly frequency dependent. Moreover, in agreement with the theoretical results, the frequency dependence of \( V/P_{\text{abs}} \) (Fig. 5 b) clearly exhibits a resonance-like behavior with the maximum at about 6 GHz. The relatively small exchange constant \( \Delta_{\text{ex}} \approx 26 \mu \text{eV} \) obtained from the observed resonant frequency nicely agrees with the recently determined exchange field of 0.2 T.\(^{35}\)

### IV. CONCLUSIONS

In conclusion, we experimentally observe a chiral charge pumping in YIG/SLG bilayers caused by the symmetry breaking at the YIG surface. Experimentally, the chiral nature of the charge pumping is manifested in the inversion of the induced dc-voltage under inversion of the applied magnetic field. The broken symmetry of the studied YIG film has been also experimentally confirmed by FMR measurements in bare YIG films. The ef-
fect provides a novel, efficient mechanism for detection of magnetization dynamics for spintronic and magnonic applications. The developed theoretical model, taking into account the exchange interaction between localized magnetic moments in YIG and itinerant spins in graphene, predicts that the strength of the effect can be increased by making use of two-dimensional conductors with a strong spin-orbital coupling, such as MoS$_2$.$^{36}$ Additionally, the found symmetry breaking can result in other, not yet observed, effects. In particular, it can enable the reciprocal effect consisting in the excitation of spin-waves of unusual symmetry via an electric current in graphene. These effects provide essentially new opportunities for the direct electrical detection and manipulation of magnetization in insulating magnetic materials and open new horizons for the emerging technologies.

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Appendix: Tilting of the exchange field

The spin rotational symmetry of graphene Hamiltonian is expressly broken by the spin-lattice coupling in Eq. (2), but it can be approximately restored in certain limit by means of a local unitary rotation of the spinor wave function. Such a gauge transformation reads as

$$U = \text{Exp} \left[-i \zeta \mathbf{b}(r) \cdot \mathbf{s} \right] \approx \mathcal{I} - i \zeta \mathbf{b}(r) \cdot \mathbf{s},$$

where $\mathbf{b}(r)$ is an axial vector, defined in Eq. (4), and $\zeta$ is a small, dimensionless parameter that we identify with

$$\zeta = \frac{a \Delta_{\text{so}}}{\hbar v_F} \ll 1.$$  

Notice that there is a gauge ambiguity in the definition of $U$. In Eq. (4), the gauge is fixed by choosing the origin of the dislocation as the lower limit of integration, but this is arbitrary. As a result, physical effects induced by the tilting of the effective exchange field appear as derivatives of $\mathbf{b}(r)$, making this approach fully consistent.

Next, we see that the unitary transformation in Eq. (A.1) gauges away the last term in the Hamiltonian of Eq. (1), generating new terms that are second order in $\zeta$ and we can safely neglect. First, we have that

$$U^\dagger \mathcal{H}_{\text{s-l}} U \approx \mathcal{H}_{\text{s-l}} - i \zeta [\mathcal{H}_{\text{s-l}}, \mathbf{b} \cdot \mathbf{s}] + \mathcal{O}(\zeta^2),$$

but note that the strength of $\mathcal{H}_{\text{s-l}}$ is already first order in $\zeta$ and therefore the second term in this last equation is actually a second order term; then, we can write

$$U^\dagger \mathcal{H}_{\text{s-l}} U \approx \mathcal{H}_{\text{s-l}} + \mathcal{O}(\zeta^2).$$

On the other hand, if we apply the unitary transformation to the kinetic term in Eq. (1) we obtain

$$-i \hbar v_F U^\dagger \mathbf{\Sigma} \cdot \partial U \approx -\frac{\hbar v_F}{a} \zeta (\partial_x u_y - \partial_y u_x) (\Sigma_x s_x + \Sigma_y s_y) + \mathcal{O}(\zeta^2) = -\mathcal{H}_{\text{s-l}} + \mathcal{O}(\zeta^2).$$

Then, the subsequent gauge field cancels out the spin-lattice coupling. To the leading in $\zeta \ll 1$ (therefore, in the strength of the interaction), the spin-lattice coupling in Eq. (2) can be understood as the non-abelian connection that transports the electron spin through the distorted crystal, following the torsion created by the screw dislocations in YIG.

We have to apply the transformation to the exchange coupling. Formally, we have

$$\Delta_{\text{ex}} U^\dagger \mathbf{m} \cdot \mathbf{s} U = \Delta_{\text{ex}} \mathbf{n} \cdot \mathbf{s},$$

where $\mathbf{n} = R \mathbf{m}$, and $R$ is a SO(3) rotation whose matrix elements read

$$R_{ij} = \frac{1}{2} \text{Tr} \left[s_i U^\dagger s_j U \right].$$

More precisely, $R$ can be written as

$$R = \text{Exp} [i \zeta \mathbf{b} \cdot \mathbf{\ell}],$$

where the SO(3) generators $\mathbf{\ell} = (\ell_x, \ell_y, \ell_z)$ in this basis read

$$\ell_x = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -2i \\ 0 & 2i & 0 \end{pmatrix},$$

$$\ell_y = \begin{pmatrix} 0 & 0 & 2i \\ 0 & 0 & 0 \\ -2i & 0 & 0 \end{pmatrix},$$

$$\ell_z = \begin{pmatrix} 0 & -2i & 0 \\ 2i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}.$$

To the leading order in $\zeta$ we have$^{37}$

$$\mathbf{n} \approx \mathbf{m} - 2 \zeta \mathbf{b} \times \mathbf{m} + \mathcal{O}(\zeta^2),$$

which corresponds to Eq. (3).
The reported voltage is then the result of the electromotive force acting on majority carriers in SLG induced by the magnetic field, in agreement with symmetry arguments. This prediction is in fact supported by preliminary experiments. A careful study of the induced transverse voltage will be a topic of our further investigations.

By plugging Eq. (3) into Eq. (6), the $\beta_1$ term generates the longitudinal voltage in Eq. (7), whereas the $\beta_2$ term leads to a transverse voltage. The latter is even in the applied magnetic field, in agreement with symmetry arguments. This prediction is in fact supported by preliminary experiments. A careful study of the induced transverse voltage will be a topic of our further investigations.

The action of the SO(3) generators over a vector $\mathbf{v}$ satisfy the following property: $(\mathbf{u} \cdot \ell) \mathbf{v} = 2i \mathbf{u} \times \mathbf{v}$. 

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