The Late-time Afterglow Evolution of Long Gamma-Ray Bursts GRB 160625B and GRB 160509A

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Received 2019 June 6; revised 2020 March 22; accepted 2020 April 6; published 2020 May 5

Abstract

We present post-jet-break Hubble Space Telescope, Very Large Array, and Chandra observations of the afterglow of the long γ-ray bursts GRB 160625B (between 69 and 209 days) and GRB 160509A (between 35 and 80 days). We calculate the post-jet-break decline rates of the light curves and find the afterglow of GRB 160625B is inconsistent with a simple \( t^{3/4} \) steepening over the break, expected from the geometric effect of the jet edge entering our line of sight. However, the favored optical post-break decline \( f_ν \propto t^{-1.96\pm0.07} \) is also inconsistent with the \( f_ν \propto t^{-p} \) declining (where \( p \approx 2.3 \)) from the pre-break light curve), which is expected from exponential lateral expansion of the jet; perhaps suggesting lateral expansion that only affects a fraction of the jet. The post-break decline of GRB 160509A is consistent with both the \( t^{3/4} \) steepening and with \( f_ν \propto t^{-p} \). We also use BOXFIT to fit afterglow models to both light curves and find both to be energetically consistent with a millisecond magnetar central engine, but the magnetar parameters need to be extreme (i.e., \( E \approx 3 \times 10^{52} \) erg). Finally, the late-time radio light curves of both afterglows are not reproduced well by BOXFIT and are inconsistent with predictions from the standard jet model; instead, both are well represented by a single power-law decline (roughly \( f_ν \propto t^{-1} \)) with no breaks. This requires a highly chromatic jet break \( (t_{j,\text{radio}} > 10 \times t_{j,\text{optical}}) \) and possibly a two-component jet for both bursts.

Unified Astronomy Thesaurus concepts: Gamma-ray bursts (629); Relativistic jets (1390)

1. Introduction

Gamma-ray bursts (GRBs) are among the most luminous transient events in the universe. Through their association with broad-lined SNe Ic (e.g., Iwamoto et al. 1998; Woosley & Bloom 2006; Hjorth & Bloom 2012), long GRBs (LGRBs; duration of the prompt γ-ray emission more than 2 s) have been established as the terminal core-collapse explosions of massive stars at cosmological distances (e.g., Paczynski 1986; Woosley 1993; MacFadyen & Woosley 1999), where an ultra-relativistic jet is launched and breaks out of the stellar envelope, generating the initial prompt emission of γ-rays through an as yet unclear mechanism (for a review on GRB physics, see, e.g., Piran 2004; Kumar & Zhang 2015). The central engine responsible for launching the jet and powering the emission may be either accretion onto a black hole formed in the core collapse (Woosley 1993) or rotational energy released through the spin-down of a nascent magnetar (e.g., Bucciantini et al. 2008, 2009). The prompt emission of a GRB is followed by an afterglow from X-ray to radio frequencies—synchrotron emission from an external shock created by the interaction between the circumburst medium (CBM) and the highly collimated and relativistically beamed jet (e.g., Paczynski & Rhoads 1993; Sari et al. 1998; Piran 2004). The flux density of the afterglow declines as a power law of the form \( f_ν \propto t^α \).

As the jet interacts with the CBM, it decelerates, and the relativistic beaming effect diminishes over time (on the order of days or weeks after an LGRB; e.g., Racusin et al. 2009). This results in a achromatic jet break in the afterglow light curve when the relativistic beaming angle (\( \Gamma^{-1} \), where \( \Gamma \) is the bulk Lorentz factor in the jet) becomes comparable to the opening angle of the jet (Rhoads 1999; Sari et al. 1999), with a steeper power-law decline after the break. The post-break decline is affected by a geometric “edge effect”, in contrast to the situation pre-break where the observer only sees a fraction of the jet front and, hence, behavior consistent with an isotropic fireball model. This phenomenon is believed to steepen the decline slope \( α \) by \(-3/4\) over the break assuming a constant-density CBM, or by \(-1/2\) in the case of a wind-like CBM (e.g., Mészáros & Rees 1999; Panaitescu & Mészáros 1999; Kumar & Zhang 2015). Another effect is that, around the same time as this happens, transverse sound waves become able to cross the jet and lateral expansion starts, exponentially decelerating the
shock wave. Theoretically, the post-break slope in this scenario is expected to be equal to $-p$ (e.g., Sari et al. 1999), where $p$ is the index of the electron Lorentz factor distribution ($\mathcal{N}(\gamma) \propto \gamma^{-p}$), typically estimated to be between 2 and 3. There is, however, evidence from numerical simulations that the lateral expansion is unimportant until a later stage—at least unless the jet is very narrow, $\theta_{\text{j}} \lesssim 3^\circ$ (Granot & Piran 2012; Lyutikov 2012). At even later times, the jet is expected to be better described as a nonrelativistic fireball in the Sedov–von Neumann–Taylor regime, resulting in a somewhat flatter decline (e.g., Frail et al. 2000; van der Horst et al. 2008).

Simulations of relativistic shocks have resulted in values around $p \approx 2.2$ (e.g., Bednár & Ostrowski 1998; Gallant et al. 1999; Kirk et al. 2000). In the X-rays, the pre-break light curve tends to follow a decline around $t^{-1.2}$ (albeit with some variation; e.g., Piran 2004; Zhang et al. 2006); thus, both of these effects result in a roughly similar post-break decline (i.e., $\sim t^{-2}$, though with high uncertainties due to the the fast decline and the resulting faintness; often there are not enough data to distinguish between $t^{-1.9}$ and $t^{-2.5}$). Thus, determining the exact scenario observationally requires late-time observations of the rapidly declining afterglows to constrain this slope.

The Large Area Telescope (LAT) on the Fermi Gamma-ray Space Telescope has detected a number of GRBs at relatively high energies (MeV–GeV) since the launch of Fermi in 2008. These are often among the most energetic GRBs, consistent with the Amati correlation between isotropic-equivalent energy $E_{\text{iso}}$ and the peak of the energy spectrum (Amati et al. 2002), and can haveisotropic-equivalent energies on the order of $10^{54}$ erg (Cenko et al. 2011). Some of these most energetic bursts do not exhibit the expected jet breaks, suggesting larger opening angles than expected and making them even more energetic intrinsically (de Pasquale et al. 2016; Gompertz & Fruchter 2017). With beamforming-corrected energies on the order of $10^{52}$ erg, magnetar spin-down models struggle to produce the required power (Cenko et al. 2011). Thus examining the late-time evolution of the LAT bursts can shed light on the physics of the most energetic GRBs.

In this paper, we present results from our late-time Hubble Space Telescope (HST), Karl G. Jansky Very Large Array (VLA) and Chandra X-ray Observatory imaging observations of the afterglows of two LAT bursts, GRB 160625B and GRB 160509A. GRB 160625B was discovered by the Gamma-ray Burst Monitor (GBM) on Fermi on 2016 June 25 at 22:40:16.28 UT (MJD 57,564.9; Dirirsa et al. 2016) and detected by the LAT as well. Xu et al. (2016) determined its redshift to be $z = 1.406$. It was one of the most energetic $\gamma$-ray bursts ever observed with $E_{\text{iso}} \sim 3 \times 10^{55}$ erg (Wang et al. 2017; Zhang et al. 2018) and a well-studied object with a multifrequency follow-up that revealed signs of a reverse shock within the jet (Alexander et al. 2017). The jet break time was unusually long, around 20 days, as expected from unusually bright GRBs (the median time is $\sim 1$ day, with more energetic bursts having longer break times; see Racusin et al. 2009). GRB 160509A was detected by GBM and LAT on 2016 May 9 at 08:59:04.36 UT (MJD 57,517.4; Longo et al. 2016a, 2016b; Roberts et al. 2016) at a redshift of $z = 1.17$ (Tanvir et al. 2016). With $E_{\text{iso}} = 8.6 \pm 1.1 \times 10^{55}$ erg, this was another luminous burst that exhibited signs of a reverse shock as well (Laskar et al. 2016).

Our observations of GRB 160625B make its follow-up one of the longest post-jet-break optical and X-ray follow-ups of a GRB afterglow, thus, providing one of the best estimates of the post-break decline in these bands so far, while for GRB 160509A, no prior estimates of the infrared/optical post-break decline could be made due to the very sparse light curve.

Our observations and data reduction process are described in Section 2. Our analysis and results are presented in Section 3. In Section 4, we discuss the implications of our findings, and finally, we present our conclusions in Section 5. All magnitudes are in the AB magnitude system (Oke & Gunn 1983), and all error bars correspond to $1\sigma$ confidence intervals. We use the cosmological parameters $H_0 = 69.6 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_m = 0.286$, and $\Omega_{\Lambda} = 0.714$ (Bennett et al. 2014).

## 2. Observations and Data Reduction

Late-time imaging observations of GRB 160625B were performed using HST/WFC3 and the F606W filter on 2016 September 5 (71.5 days) and 2016 November 13 (140.2 days). A template image of the host galaxy was created by combining images obtained with the same setup on 2017 November 6 (498.3 days) and 11 (503.6 days). At this time, the contribution of the afterglow itself was a factor of $\sim 13$ fainter than at 140 days, assuming a $f_{\gamma} \propto t^{-\alpha}$ decline where $\alpha = -2$. Imaging of GRB 160509A in the $H$ band was performed using the Canarias InfraRed Camera Experiment (CIRCE; Eikenberry et al. 2018) instrument on Gran Telescopio Canarias (GTC) on 2016 May 15 (5.8 days) and 2016 June 3 (24.8 days). Late-time imaging of GRB 160509A was done using HST/WFC3 and the F110W and F160W filters on 2016 June 13 (35.3 days); template images of the host galaxy in these filters were obtained on 2017 July 5 (422.1 days), when, assuming $\alpha = -2$, the afterglow was a factor of 143 fainter. Our HST observations of both bursts were executed as part of program GO 14353 (PI Fruchter), and these data are available at 10.17909/t9-yvpg-xf33 (GRB 160625B) and 10.17909/t9-1lx-cv41 (GRB 160509A).

Basic reduction and flux calibration of the HST images was performed by the HST CALWF3 pipeline. The calibrated images were corrected for distortion, drizzled (Fruchter & Hook 2002), and aligned to a common world coordinate system using the astrodazzle, tweakreg, and tweakback tasks in the DRIZZLEPAC package in PYTHON. The two epochs of GRB 160625B in 2017 November were combined into one template image. Subtraction of the template images and aperture photometry of the afterglows were done using IRAF. Basic reduction of the GTC/CIRCE data was done using standard IRAF tasks. The HST F160W template image was subtracted from the CIRCE images using the ISIS 2.2 package (Alard & Lupton 1998; Alard 2000). Flux calibration was done using field stars in the Two-Micron All Sky Survey catalog (Skrutskie et al. 2006), and aperture photometry was performed using standard IRAF tasks. At 24.8 days, we were unable to...
detect the afterglow and only obtained a (3σ) limit of $H \geq 21.9$ mag.

The measured magnitudes of GRB 160625B were corrected for over-subtraction caused by the continued presence of a faint afterglow in the template image. Assuming a post-jet-break decline of $\alpha = -2.0 \pm 0.2$ (obtained from a single power-law fit to uncorrected $>25$ days data, with errors rounded up to be conservative), the afterglow flux present in the template image was estimated to be $2.0 \pm 1.0\%$ of the flux at 71.5 days or $7.5 \pm 2.6\%$ of the flux at 140.2 days, and thus, the images at these epochs were over-subtracted by approximately these amounts. The magnitudes were adjusted for this; the errors of the corrected magnitudes include an estimate of the uncertainty of the over-subtraction. The magnitudes of GRB 160509A were not corrected, as the contribution of the afterglow in the template image was only estimated to be $0.7\%$ of the 35.3 days brightness. The log of optical observations and measured and corrected magnitudes of GRB 160625B are presented in Table 1, while Table 2 contains the near-infrared observations of GRB 160509A. Figure 1 shows our F606W band images and the resulting template subtractions of GRB 160625B, while Figure 2 shows the F160W image and subtraction of GRB 160509A.

Late-time X-ray imaging of both GRBs was performed using Chandra/ACIS-S in VFaint mode (proposal ID 17500753, PI Fruchter). GRB 160625B was observed on 2016 September 3 (69.8 days), 2016 November 15 (142.3 days), and 2016 November 19 (146.2 days). The latter two epochs were combined to obtain the flux at 144.3 $\pm 2.2$ days, as the flux of the afterglow was not expected to vary significantly over a few days at this time. GRB 160509A was observed on 2016 June 20 (42.1 days). Reprocessing of the Chandra level 1 data was performed using the chandra_repro script within the CIAO v. 4.9 software (CALDB v. 4.7.7; Fruscione et al. 2006), and aperture photometry was done using IRAF. The web-based Portable Interactive Multi-Mission Simulator (PIMMS\(^{20}\)) was used to convert count rates in the 0.3–10 keV range to unabsorbed flux densities at 5 keV. For GRB 160625B, we used a Galactic neutral hydrogen column density $N_{\text{HI,MW}} = 9.76 \times 10^{20}\text{ cm}^{-2}$ (Willingale et al. 2013), a photon index of $\Gamma_{X} = 1.86$, and an intrinsic absorption of $N_{\text{HI,int}} = 2.1 \times 10^{21}\text{ cm}^{-2}$ as derived by Alexander et al. (2017). These parameters are also consistent with the initial analysis by Melandri et al. (2016). For GRB 160509A, we used a Galactic neutral hydrogen column density $N_{\text{HI,LMW}} = 2.12 \times 10^{21}\text{ cm}^{-2}$ (Willingale et al. 2013), a photon index of $\Gamma_{X} = 2.07$ and an intrinsic absorption of $N_{\text{HI,int}} = 1.52 \times 10^{22}\text{ cm}^{-2}$, following Laskar et al. (2016). $\Gamma_{X}$ is assumed to be constant over the light-curve break. The log of the X-ray observations and derived flux densities is presented in Table 3.

GRB 160625B was observed in the radio using the VLA in the C, K, X, and/or $K_{\beta}$ bands at five epochs between 2016 March 30 (4.5 days) and 2017 January 20 (209.0 days), and GRB 160509A in the C and X bands on 2016 June 2 (23.9 days), 2016 June 15 (36.9 days), and 2016 July 28 (79.9 days) (program IDs S81117 and SH0753, PI Chenko and Fruchter, respectively). The observations were done in the B configuration, apart from the last GRB 160625B point where configuration A was used. The log of our observations is presented in Table 4. The data were reduced using the Common Astronomy Software Applications package (CASA; McMullin et al. 2007).\(^{21}\) Calibration was carried out using the standard VLA calibration pipeline provided in CASA. For GRB 160625B, we used J2049+1003 as our complex gain calibrator and 3C48 as our flux and bandpass calibrator. For GRB 160509A, we used J2005+7752 as our complex gain calibrator and 3C48 as our flux and bandpass calibrator. After calibration, the data were manually inspected for radio-frequency interference flagging. Imaging was carried out using the clean algorithm in interactive mode in CASA. Flux densities reported in Table 4 correspond to peak flux densities measured in a circular region centered on the GRB position, with radius comparable to the nominal FWHM of the VLA synthesized beam in the appropriate configuration and frequency band. The reported errors include the VLA

\(^{20}\) https://heasarc.gsfc.nasa.gov/docs/software/tools/pimms.html

\(^{21}\) https://casa.nrao.edu

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**Table 1**

Log of Our Late-time HST/WFC3 Observations of GRB 160625B

| Phase (days) | MJD  | $t_{\text{exp}}$ (s) | F606W (mag) | Corrected F606W (mag) |
|-------------|------|---------------------|-------------|-----------------------|
| 71.5        | 57636.4 | 2400               | 25.38 ± 0.03 | 25.36 ± 0.04          |
| 140.2       | 57705.1 | 4800               | 26.76 ± 0.06 | 26.67 ± 0.07          |
| 498.3       | 58063.2 | 4800               | ...         | ...                   |
| 503.6       | 58068.5 | 4800               | ...         | ...                   |

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**Figure 1.** Afterglow and host galaxy of GRB 160625B in the F606W band. Panel (a): the afterglow and the host galaxy at 71.5 days; panel (b): 140.2 days; panel (c): the combined template at $<500$ days; panel (d): the template-subtracted image at 71.5 days; and panel (e): the subtraction at 140.2 days. North is up and east is to the left in all panels. The black north–south line corresponds to one arcsecond. The afterglow location is indicated with red tick-marks.

**Figure 2.** Afterglow and host galaxy of GRB 160509A in the F160W band. Panel (a): the afterglow and the host galaxy at 35.3 days; panel (b): the template-subtracted image at 35.3 days. North is up and east is to the left in all panels. The black north–south line corresponds to one arcsecond. The afterglow location is indicated with red tick-marks. The afterglow is very weak compared to the host galaxy, making a template subtraction crucial for this target.
The Astrophysical Journal, 894:43 (14pp), 2020 May 1

Kangas et al.

Table 2
Log of Our Late-time HST/WFC3 and GTC/CIRCE Observations of GRB 160509A

| Phase (days) | MJD    | $t_{\text{exp,F110W}}$ (s) | F110W (mag)     | $t_{\text{exp,F160W}}$ (s) | F160W (mag)     | $t_{\text{exp,H}}$ (s) | $H$ (mag) |
|--------------|--------|----------------------------|-----------------|-----------------------------|-----------------|-----------------------|-----------|
| 5.8          | 57523.2| ...                        | ...             | ...                         | ...             | ...                   | 20.50 ± 0.17 |
| 24.8         | 57542.2| ...                        | ...             | ...                         |     ...         | ...                   | ≥21.9     |
| 35.3         | 57552.7| 2697                       | 27.11 ± 0.10    | ...                         |     ...         | ...                   | ...        |
| 422.1        | 57939.5| 2697                       | ...             | 2797                        | 26.07 ± 0.07    | ...                   | ...        |

Table 3
Log of Our Late-time Chandra/ACIS-S Observations of GRB 160625B and GRB 160509A

| Phase (days) | MJD    | $t_{\text{exp}}$ (ks) | $f_\nu$ (5 keV) (erg s$^{-1}$ cm$^{-2}$ keV$^{-1}$) |
|--------------|--------|-----------------------|--------------------------------------------------|
| 160625B      |        |                       |                                                  |
| 69.8         | 57634.7| 19.80                 | (1.47 ± 0.29) × 10$^{-15}$                        |
| 142.3        | 57707.3| 45.84                 | ...                                               |
| 144.3 ± 2.2  | 57709.3| 69.56                 | (3.21 ± 0.79) × 10$^{-16}$                        |
| 146.2        | 57711.2| 23.72                 | ...                                               |
| 160509A      |        |                       |                                                  |
| 42.1         | 57559.5| 24.75                 | (1.38 ± 0.25) × 10$^{-15}$                        |

Note. *Combination of the 142.3 and 146.2 days epochs.

Table 4
Log of Our VLA Observations of GRB 160625B and GRB 160509A

| Phase (days) | MJD    | $\nu$ (GHz) | $f_\nu$ ($\mu$Jy) | Configuration |
|--------------|--------|-------------|-------------------|---------------|
| 160625B      |        |             |                   |               |
| 4.5          | 57569.4| 4.8         | 104 ± 16           | B             |
| 4.5          | 57569.4| 7.4         | 454 ± 27           | B             |
| 4.5          | 57569.4| 19          | 278 ± 5            | B             |
| 4.5          | 57569.4| 25          | 204 ± 36           | B             |
| 13.4         | 57578.3| 4.8         | 377 ± 25           | B             |
| 13.4         | 57578.3| 7.4         | 310 ± 21           | B             |
| 13.4         | 57578.3| 22          | 163 ± 20           | B             |
| 31.3         | 57596.2| 7.4         | 113 ± 16           | B             |
| 31.3         | 57596.2| 22          | 88 ± 19            | B             |
| 58.3         | 57623.2| 6.1         | 75 ± 11            | B             |
| 58.3         | 57623.2| 22          | 52 ± 13            | B             |
| 209.0        | 57773.9| 6.1         | 16 ± 5             | A             |
| 160509A      |        |             |                   |               |
| 23.9         | 57541.3| 6.0         | 80 ± 8             | B             |
| 23.9         | 57541.3| 9.0         | 71 ± 7             | B             |
| 36.9         | 57554.3| 5.0         | 50 ± 7             | B             |
| 36.9         | 57554.3| 6.9         | 52 ± 7             | B             |
| 36.9         | 57554.3| 8.5         | 41 ± 6             | B             |
| 36.9         | 57554.3| 9.5         | 29 ± 6             | B             |
| 79.9         | 57597.3| 6.0         | 27 ± 6             | B             |
| 79.9         | 57597.3| 9.0         | 25 ± 5             | B             |

Note. The GRB 160625B points until 31.3 days were also reported in Troja et al. (2017) but without the calibration uncertainty.

3. Analysis

3.1. GRB 160625B

As our HST observations took place after the jet break, we combined our data set with earlier ground-based observations. Both Alexander et al. (2017) and Troja et al. (2017) have published Sloan Digital Sky Survey $r'$ band light curves of GRB 160625B. However, there is a slight (~0.1 mag) systematic offset between these data, so in our light curve fits, we have only used the Troja et al. (2017) data set, which has a larger number of data points and which was directly tied to the PanSTARRS magnitude system. Magnitudes of GRB 160625B in the $r'$ band were converted to flux density at the central wavelength of the F606W filter (5947 Å) assuming a spectral slope of $f_\nu \propto \nu^{-0.68}$ between the characteristic synchrotron frequency $\nu_B$ and the cooling frequency $\nu_c$ (Alexander et al. 2017). As the optical spectrum with $\beta = -0.68 ± 0.07$ is consistent with the expected index of $\beta = 0.65$ when $p = 2.3$ (also consistent with the light curve; see Section 4.2.1), host extinction is assumed to be negligible. Optical fluxes have been corrected for Galactic reddening, $E(B – V) = 0.1107$ mag (Schlafly & Finkbeiner 2011), assuming the Cardelli et al. (1989) extinction law. In the X-ray, we combined our Chandra data with the GRB 160625B light curve from the Swift/XRT light-curve repository23 (Evans et al. 2007, 2009), converted to 5 keV flux densities using PIMMS as described in Section 2.

3.2. GRB 160509A

As our HST observations took place after the jet break, we combined our data set with earlier ground-based observations. Both Alexander et al. (2017) and Troja et al. (2017) have published Sloan Digital Sky Survey $r'$ band light curves of GRB 160509A. However, there is a slight (~0.1 mag) systematic offset between these data, so in our light curve fits, we have only used the Troja et al. (2017) data set, which has a larger number of data points and which was directly tied to the PanSTARRS magnitude system. Magnitudes of GRB 160509A in the $r'$ band were converted to flux density at the central wavelength of the F606W filter (5947 Å) assuming a spectral slope of $f_\nu \propto \nu^{-0.68}$ between the characteristic synchrotron frequency $\nu_B$ and the cooling frequency $\nu_c$ (Alexander et al. 2017). As the optical spectrum with $\beta = -0.68 ± 0.07$ is consistent with the expected index of $\beta = 0.65$ when $p = 2.3$ (also consistent with the light curve; see Section 4.2.1), host extinction is assumed to be negligible. Optical fluxes have been corrected for Galactic reddening, $E(B – V) = 0.1107$ mag (Schlafly & Finkbeiner 2011), assuming the Cardelli et al. (1989) extinction law. In the X-ray, we combined our Chandra data with the GRB 160509A light curve from the Swift/XRT light-curve repository23 (Evans et al. 2007, 2009), converted to 5 keV flux densities using PIMMS as described in Section 2.

22 http://www.swift.ac.uk/xrt_curves/
23 [https://science.mrao.ac.uk/facilities/vla/docs/manuals/oss/performance/fdscale]
Table 5
Parameters of Our Best Smooth Broken Power-law and Single Power-Law Fits to the GRB 160625B Light Curves

| Parameter | $\omega = 3$ | $\omega = 10$ | Single Power Law |
|-----------|-------------|---------------|-----------------|
| $t_b$,F606W | $24 \pm 3$ days | $17 \pm 2$ days | $17 \pm 4$ days |
| $\alpha_{1,F606W}$ | $-0.96 \pm 0.01$ | $-0.96 \pm 0.01$ | $-0.97 \pm 0.01$ |
| $\alpha_{2,F606W}$ | $-2.27 \pm 0.13$ | $-1.96 \pm 0.07$ | $-1.94 \pm 0.13$ |
| Reduced $\chi^2$ | 5.5 | 4.4 | 1.8 |
| $t_b$,X | $27 \pm 5$ days | $22 \pm 4$ days | $22 \pm 5$ days |
| $\alpha_{1,X}$ | $-1.24 \pm 0.02$ | $-1.24 \pm 0.02$ | $-1.25 \pm 0.03$ |
| $\alpha_{2,X}$ | $-2.40 \pm 0.19$ | $-2.23 \pm 0.15$ | $-2.20 \pm 0.13$ |
| Reduced $\chi^2$ | 0.91 | 0.81 | 0.84 |

Note. The bump(s) between 8.5 and 26.5 days were ignored in the single power-law fits to the early and late decline.

$\omega = 10$. The optical and X-ray light curves and our best fits in both cases are shown in Figure 3.

We also fitted the decline using a single power law before 8.5 days and another after 26.5 days, ignoring the points in the vicinity of the break itself. The $r'$ band light curve contains at least one smooth “bump” feature, possibly two depending on $t_b$ (we discuss the nature of the bump in Section 4.1). These may disturb the optical broken power-law fits; the reduced $\chi^2$ values of these fits are rather high; although, the small errors also contribute to this. The result is $\alpha_{2,F606W} = -1.94 \pm 0.13$, nearly exactly coincident with the $\omega = 10$ case but with a $\sim 2.5\sigma$ difference to $\omega = 3$. Repeating this in the X-ray results in $\alpha_{2,X} = -2.20 \pm 0.13$, which is also almost identical to the $\omega = 10$ case. A simultaneous single power-law fit to both post-break light curves results in $\alpha_2 = -2.01 \pm 0.09$.

Assuming an achromatic break, we determined $t_b$ by taking the weighted average of $t_b$,F606W and $t_b$,X. In the $\omega = 10$ case, the result is $t_b = 19 \pm 2$ days. Assuming an instantaneous break (corresponding to $\omega = \infty$) between the single power-law fits, the resulting jet break times are consistent, $t_b$,F606W = $17 \pm 4$ days and $t_b$,X = $22 \pm 5$ days, and the weighted average $t_b = 19 \pm 3$ days. In the $\omega = 3$ case, we obtained $t_b = 25 \pm 3$ days.

For the radio light curve of GRB 160625B, we combined flux measurements from Alexander et al. (2017) and Troja et al. (2017) with our own data. At 58.3 and 209.0 days, we have observations at 6.1 GHz; we therefore obtained flux densities at 6.1 GHz by power-law interpolation between 5 and 7.1 GHz literature values at 22.5 and 48.4 days. We also scaled the 7.4 GHz flux at 31.34 days assuming the same power law as at 22.5 days. Points earlier than 22.5 days were ignored in the analysis of the late afterglow due to the influence of the reverse shock (Alexander et al. 2017). The resulting best fit for the late-time light curve is $\alpha_{6,1GHz} = -1.08 \pm 0.11$ as shown in Figure 3.

Additionally, we used the BOXFIT v.2 afterglow fitting code (van Eerten et al. 2012), based on the Afterglow Library. 24 to fit the light curve. The library of models itself was constructed using the relativistic hydrodynamics code RAM (Zhang & MacFadyen 2006). BOXFIT then uses a downhill simplex method with simulated annealing to find the best fit, interpolating between these models. We omitted the pre-break radio points due to the influence of the reverse shock in the early light curve and all of the radio points below 5 GHz due to possible strong Milky Way scintillation (Alexander et al. 2017). We also included the ultraviolet to near-infrared frequency data from Troja et al. (2017). We assumed a CBM of the interstellar medium (ISM) type (the light curve rules out a wind-type CBM; see Section 4.2.1) and performed the fit with three different values of the participation fraction $\xi$, i.e., the fraction of electrons accelerated by the shock into a nonthermal power-law distribution. Simulations indicate that this value can be as low as 0.01 (Sironi & Spitkovsky 2011; Sironi et al. 2013; Warren et al. 2018); we used fixed values of 1 (commonly assumed in the literature), 0.1, and 0.01. All other model parameters were allowed to vary within the full range allowed by BOXFIT. The resulting best-fit parameters are summarized in Table 6. Taking the isotropic-equivalent $\gamma$-ray energy $E_{iso} = 3.0 \times 10^{54}$ erg (with the fluence from Svinkin et al. 2016), we also calculate the geometry-corrected total energy and the efficiency $\eta = E_{iso}/(E_{K,iso} + E_{iso})$ for the conversion of kinetic energy to $\gamma$-rays. These fits, however, fail to reproduce the measured power-law slope of $\alpha_{6,1GHz} = -1.08 \pm 0.11$, instead predicting a break in the radio light curve around ~100 days (associated with the passage of $\nu_m$ through this band). See Figure 4 for our best BOXFIT light-curve fits. For clarity, we plot the $U$, F606W, and $H$ bands, covering the optical/infrared behavior from early to late times, but we omit the other optical/infrared bands, which exhibit very similar behavior (see Troja et al. 2017). While the late-time 6.1 GHz light curve can be reproduced slightly better at low $\xi$ values, the fit at higher frequencies or earlier times is still somewhat worse; we show 22 GHz as an example.

As some optical and X-ray observations are nearly contemporaneous, we can construct the spectral energy distribution (SED) of GRB 160625B. Figure 5 shows the SED at four epochs around or after the break, along with spectra predicted by BOXFIT at these epochs. The power-law slope of the SED, $\beta$, between the optical ($r$) and X-ray (5 keV) bands, steepens slightly over time, from $-0.79 \pm 0.02$ between

http://cosmo.nyu.edu/afterglowlibrary/index.html
Table 6
Best-fit Physical Parameters of the Best BOXFIT Fits to GRB 160625B

| Parameter   | $\xi = 1$ | $\xi = 0.1$ | $\xi = 0.01$ |
|-------------|-----------|-------------|-------------|
| $p$         | 2.30      | 2.05        | 2.05        |
| $E_{\text{K,iso}}$ (erg) | $1.8 \times 10^{54}$ | $1.4 \times 10^{54}$ | $1.3 \times 10^{55}$ |
| $\xi_0$     | 0.13      | 0.25        | 0.024       |
| $\nu$ (cm$^{-3}$) | $1.1 \times 10^{-5}$ | 0.18        | 0.96        |
| $\theta_\gamma$ (rad) | 0.059      | 0.14        | 0.13        |
| $\theta_\text{obs}$ (deg) | 3.4        | 7.8         | 7.2         |
| $\theta_\text{obs}$ (rad) | 0.012      | $1.1 \times 10^{-3}$ | $1.1 \times 10^{-3}$ |
| $\chi^2$/dof | 8.6        | 4.6         | 4.5         |

$E_{\text{tot}}$ (erg) $= 8.3 \times 10^{51}$, $4.1 \times 10^{52}$, $1.3 \times 10^{53}$.

3 and 10 days to $-0.86 \pm 0.04$ at 141 days. This is steeper than $-0.65$, expected from $p \approx 2.3$ implied by the early optical and X-ray light curves (see Section 4.2.1) for $\nu < \nu_c$, but shallower than $-1.15$, which is expected for $\nu > \nu_c$. Alexander et al. (2017) obtained an early X-ray spectral slope similar to this, $\beta_X = -0.86^{+0.09}_{-0.10}$, and explained this as $\nu_c$ being located just below the X-ray band. However, according to the UKSSDC Swift Burst Analyzer, the X-ray photon index $\Gamma_X$ (and, thus, the spectral slope in X-ray) does not significantly evolve over the first 30 days but stays around $\sim 1.8$, after which the spectrum seems to flatten to $\Gamma_X \sim 1.1$. This feature may not be real, though, as the Burst Analyzer light curve deviates much more from a clean power law when this is used in flux calculation—thus, we assume a constant $\Gamma_X$. If $\nu_c$ was initially just below X-ray and changed as $\nu_c \propto 1/\nu^2$, one would expect the spectrum to instead steepen over time to its $\nu \gg \nu_c$ value. We discuss this evolution further in Section 4.2.1.

3.2. GRB 160509A

It was noted in Laskar et al. (2016) that the host galaxy of GRB 160509A contributes substantially to the optical and infrared photometry and that the event occurred behind a significant amount of extinction in the host galaxy. In order to estimate the host galaxy extinction along the line of sight to the GRB, we removed the foreground Galactic reddening of $E(B - V) = 0.2519$ mag (Schlafly & Finkbeiner 2011) using the Cardelli et al. (1989) law, and we assumed an $f_\nu \propto \nu^\beta$ SED, where $\beta = -0.6$ (consistent with $\nu < \nu_c$ and $p \approx 2.2$, determined based on the X-ray spectrum and light curve by Laskar et al. 2016). For the host, we assume the Pei (1992) extinction law for the Small Magellanic Cloud (SMC), as both Kann et al. (2006) and Schady et al. (2012) found the extinction curve in the SMC to be consistent with their samples. We fitted the observed optical-infrared SED simultaneously at two epochs, corrected using this extinction curve, to find the required extinction correction to match $\beta = -0.6$. The GRB flux in the $g'$ band at 1 day was estimated by subtracting the observed flux at 28 days ($g' = 25.39 \pm 0.12$; Laskar et al. 2016) from the flux at 1.0 days ($g' = 25.03 \pm 0.15$; Cenko et al. 2016). The host is assumed to dominate at 28 days due to the flatness of the light curve even after the X-ray break. In the $J$ band, we subtracted the flux of the host galaxy measured in the HST F110W filter (using a 1″ aperture) from the flux at 1.2 days ($J \approx 19.7$; Tanvir et al. 2016). The $r'$ band was not included in the SED, as the late and early fluxes are consistent within $1\sigma$ (Cenko et al. 2016; Laskar et al. 2016). Our F110W and F160W observations at 35.3 days made up the other epoch to be fitted simultaneously. The resulting host extinction is...
the indicated participation fraction $\xi$ using a constant CBM density profile are shown. Data denoted by gray points are ignored in the fitting (see the text).

$A_V = 2.8 \pm 0.1$ mag in the rest frame (this is somewhat lower than the result obtained by Laskar et al. 2016, using an afterglow model fit where the host flux was a free parameter). Using the Pei (1992) law, the extinction correction in F160W (approximately $i$-band in the rest frame) is thus 1.5 mag. In the Milky Way, the adopted $N_{H,\text{int}} = 1.52 \times 10^{22}$ cm$^{-2}$ would correspond to $A_V \approx 6.9$ mag (Güver & Özel 2009), suggesting a low $A_V/N_{H}$ ratio by Milky Way standards but higher than that of most GRB hosts. This ratio is consistent with the $A_V$ versus $N_{H}/A_V$ relation in Krühler et al. (2011). As in the case of GRB 160625B, we combined our Chandra data of GRB 160509A with the data from the Swift/XRT light-curve repository converted to 5 keV flux densities.

The CIRCE $H$-band fluxes were converted to the narrower F160W filter assuming $\beta = -0.6$. The F160W and X-ray data and our power-law fits are presented in Figure 5, and the parameters of the fits are listed in Table 7. For our power-law fits, we ignore the data points before ~0.5 days ($4 \times 10^4$ s), as the early X-ray light curve may contain a plateau and/or a flare; see Figure 6. In this case, the smooth- and sharp-break scenarios give similar results: the best fit for the post-break decline for $\omega = 3$ is $\alpha_{1,\text{X}} = -1.98 \pm 0.10$ and for $\omega = 10$, $\alpha_{2,\text{X}} = -1.96 \pm 0.09$. The jet-break times, 3.2 ± 0.9 days and $3.7 \pm 0.8$ days, respectively, are consistent with each other as well.

In the radio, we obtained the fluxes at 6 and 9 GHz at the epochs earlier than 79.9 days by power-law interpolation between observed fluxes—our measurements at 36.9 days and those published in Laskar et al. (2016) at earlier times. We then fitted a single power law to the points where the reverse shock should no longer dominate the radio flux (i.e., $\geq 10$ days; Laskar et al. 2016). The resulting decline slopes are $\alpha_{6\text{GHz}} = -0.91 \pm 0.11$ and $\alpha_{9\text{GHz}} = -0.92 \pm 0.13$. Since

| Parameter  | $\omega = 3$ | $\omega = 10$ |
|------------|--------------|--------------|
| $f_{\gamma,\text{X}}$ | 3.2 ± 0.9 days | 3.7 ± 0.8 days |
| $\alpha_{1,\text{X}}$ | $-1.06 \pm 0.10$ | $-1.20 \pm 0.06$ |
| $\alpha_{2,\text{X}}$ | $-1.98 \pm 0.10$ | $-1.96 \pm 0.09$ |
| Reduced $\chi^2$ | 0.84 | 0.85 |
the reverse shock may still be contributing a nonnegligible fraction of the flux at 10 days, we also performed the fit without this epoch. The results are consistent but less constraining: $\alpha_{\text{obs}} = -1.07 \pm 0.18$ and $\alpha_{\text{9GHz}} = -0.92 \pm 0.21$. The slopes at other frequencies between 5 and 16 GHz, fitted from 10 to 20 days, are all consistent with these, ranging from $-0.80 \pm 0.10$ (7.4 GHz) to $-1.02 \pm 0.04$ (8.5 GHz). In F160W and/or $H$, we only have two points and an upper limit; therefore, we simply measure the decline assuming a single power law. As the first point at 5.8 days is after the jet break time we obtained from the X-ray fit, there should be no significant deviation from a single power law. The measured decline is $\alpha_{\text{obs}} = -2.09 \pm 0.10$, consistent within 1σ with the X-ray decline.

Using BOXFIT, we again fitted the light curve at three different values of $\xi$: 1, 0.1, and 0.01. As with the power-law fits, the X-ray points before 0.6 days were ignored, since BOXFIT cannot accommodate continuous energy injection. Radio points with a significant reverse shock contribution were also ignored (i.e., <10 days; at frequencies <5 GHz also 10.03 days; see Laskar et al. 2016). We ran BOXFIT with the boosted-frame wind-like CBM model (with both strong and medium boost) and a lab-frame model with ISM-like CBM, as the lack of optical data makes it difficult to distinguish between different CBM profiles (although the ISM scenario is tentatively favored by Laskar et al. 2016). However, as shown in Figure 7, our fits in a wind CBM do not reproduce the jet break clearly detected in the X-ray light curve. Even with the parameters in Laskar et al. (2016), the break only appears at $\sim$100 days, and the X-ray fit is much worse than with an ISM-type CBM. Thus, the analytical model and BOXFIT seem to disagree on how the jet behaves in a wind-type CBM, and we concentrate on the ISM scenario. The best ISM fits are shown in Figure 8; Figure 9 shows the SED at three post-break epochs along with spectra produced by BOXFIT at these epochs. Our resulting best-fit parameters are summarized in Table 8. These fits (including the wind fits) again fail to match the observed shape of the radio light curve, although the amplitude of the flux can be reproduced at some epochs.

4. Discussion

4.1. The Shape of the Break

In the X-ray, we find little difference in the reduced $\chi^2$ values of the fits between a sharp and a smooth break for GRB160625B. In the optical, however, fixing $\omega = 3$ results in a visible and significant residual of 4.2σ at 140.2 days, while fixing $\omega = 10$ results in a residual of 1.5σ. The reduced $\chi^2$ of the latter fit is also slightly smaller. In the optical light curve, one can see either one slight bump or two, depending on the break time. These deviations from a perfect power law may disturb the fit and cause the high $\chi^2$ values, which suggests that one should also try only using the post-break points. Simply fitting a single power law to the points after 26.5 days results in a consistency with the $\omega = 10$ case. We thus conclude that while both values of $\omega$ remain plausible, a sharp break with $\omega = 10$ is more likely. A sharp break also implies a small viewing angle $\theta_{\text{obs}}$ (Ryan et al. 2015), which is compatible with the BOXFIT results for this burst.

The post-jet-break decline of GRB 160625B has been previously estimated to be $j_f \propto t^{-2}$, where generally $\alpha_2 \sim -2.3$, and its error is roughly 0.5 (Alexander et al. 2017; Friaj et al. 2017; Lü et al. 2017). These estimates are largely consistent with both sharp and smooth breaks (and with our results listed in Table 5). However, all of these results are based on observations no later than $\sim$50 days from the burst ($\sim 2.5 \times t_j$, compared to our latest observations at $\sim 7 \times t_j$), and their post-break fluxes mostly include relatively large uncertainties. In addition, Troja et al. (2017) obtained a more precise post-break slope of $\alpha_2 = -2.57 \pm 0.04$, and Strausbaugh et al. (2018) obtained $\alpha_{2,\text{optical}} \approx 1.6$ and $\alpha_{2,X} = -2.06 \pm 0.22$, but their optical slope is inconsistent with our later-time optical data in both cases.

Troja et al. (2017) placed their estimate of the jet break at 14 days, during the “bump” in the light curve between $\sim$8 days and $\sim$16 days. Using the same data, Strausbaugh et al. (2018) suggested a break at 12.6 days at the peak of the bump, which they took as brightening of the jet toward its edges. However, our later-time data require a later break and a steeper $\omega_2$, leading us to suggest that the bump may still be due to angular brightness differences or perhaps the result of density fluctuations in the CBM, but not necessarily a sign of a bright edge—and seemingly not simultaneous with a true jet break. The bump is not seen in the X-rays, which is also consistent with a density fluctuation, as the flux above $\nu_c$ is insensitive to ambient density (Kumar 2000). Strausbaugh et al. (2018) also suggest that a slowly changing spectral slope in the optical bands indicates a gradual cooling transition instead of a $\nu_c$ break in the spectrum and that the optical spectrum eventually becomes consistent with $\beta \sim -1.1$, i.e., the slope above $\nu_c$, which would disfavor a CBM density fluctuation because of this insensitivity. We, however, measure $\beta = -0.86 \pm 0.04$ between F606W and 5 keV at 141 days, suggesting that $\nu_c$ is still above optical frequencies but below X-ray at this time. Thus, we cannot rule out either scenario for the bump, but we can place the jet break at an epoch after the bump.

In the case of GRB 160509A, the $\chi^2$ values of the fits with different $\omega$ are close to equal and the post-break slopes are in agreement. A higher $\omega_{\text{obs}}$ results in a softer break (Ryan et al. 2015); so in this case, considering that $\theta_{\text{obs}} \sim 0.6\theta_J$ (from BOXFIT), one would expect the break to be softer than for GRB 160625B where $\omega_{\text{obs}}$ is much smaller or close to zero. One can attempt to resolve this by finding inconsistencies in estimates of $p$ based on the pre-break light curve and spectrum. The X-ray spectrum, with a slope of $\beta = -1.07 \pm 0.04$, is consistent with
\( p \approx 2.2 \) and with \( \nu_c \) being below the X-ray band (Laskar et al. 2016). As a result, we can use \( \alpha = (2-3p)/4 \) independent of the CBM distribution (Granot & Sari 2002); in the case of \( \omega = 3 \), we obtain \( p = 2.08 \pm 0.14 \) and for \( \omega = 10 \), \( p = 2.27 \pm 0.08 \). While the former is closer to the measured post-break decline, both values are consistent with 2.2.

4.2. Physical Implications

4.2.1. GRB 160625B

Based on the well-constrained pre-break light curve of the afterglow of GRB 160625B, one can estimate the electron energy distribution index \( p \); below the cooling frequency \( \nu_c \), in the case of a wind-like CBM, \( \alpha_{\text{wind}} = (1-3p)/4 \), while for a
constant-density CBM similar to the ISM, $\alpha_{\text{ISM}} = 3(1-p)/4$ (Granot & Sari 2002). Thus, in the optical, one obtains $p = 1.63 \pm 0.02$ in the wind case and $p = 2.29 \pm 0.06$ in the ISM case. Above $\nu_c$, in both cases, $\alpha = (2-3p)/4$. Comparing the optical and X-ray spectra and fluxes, Alexander et al. (2017) argue that $\nu_c$ lies below the X-ray frequencies after $\sim 1.2 \times 10^5$ s, and thus, the early X-ray light curve gives us $p = 2.29 \pm 0.06$. This is also consistent with the spectrum below the X-ray frequencies (Alexander et al. 2017), and thus, as the $p$ values in the wind scenario are mutually inconsistent, an ISM-like density profile is favored. Fraija et al. (2017) infer a transition from wind-like to ISM-like CBM at $\sim 8000$ s.

When only taking into account the relativistic visible-edge effect (Mészáros & Rees 1999), the slope of the decline is expected to steepen in the jet break by a factor of $t^{-3/4}$ in a constant-density CBM. In the $\omega = 10$ case, the difference between the pre- and post-break power laws is $\Delta f_{\text{FWHM}} = -1.00 \pm 0.08$ in the optical and $\Delta f_{\text{AX}} = -0.99 \pm 0.16$ in the X-ray. Thus, a $t^{-3/4}$ factor can be ruled out in the optical at a $>3\sigma$ level (although in the X-ray, only at a $\sim 1.5\sigma$ level). The difference is larger in the $\omega = 3$ case ($>4\sigma$ and $>2\sigma$, respectively), and therefore, a simple edge effect is inconsistent with our observations regardless of whether the break is sharp or smooth (the $t^{-1/2}$ factor from a wind-like CBM is, of course, even less plausible).

If one assumes a smooth break ($\omega = 3$), both the optical and X-ray post-break decline rates are consistent with the form $f_\nu \propto t^{-\beta}$, for $p \approx 2.3$, as expected from exponential lateral expansion (Rhoads 1999; Sari et al. 1999). At first glance, the favored sharp-break scenario seems to make GRB 160625B inconsistent with an $f_\nu \propto t^{-\beta}$ decline in the optical band (the X-ray slope is still consistent with it) and would seem to require another physical mechanism. One explanation could be that the true jet break is due to a combination of the visible-edge effect and more limited lateral expansion. The steepening in both bands is a factor of $t^{-1}$, steeper than the $t^{-3/4}$ expected from the edge effect (Mészáros & Rees 1999; Panaitescu & Mészáros 1999), and the resulting $\alpha_2$ values are only consistent within $2\sigma$, while the full exponential lateral expansion scenario described by Rhoads (1999) should result in identical slopes. In some numerical simulations, lateral expansion has been found to initially involve only the outer layer of the jet carrying a fraction of its energy, and the bulk of the material remains unaffected for some time (van Eerten & MacFadyen 2012), while the results of Rhoads (1999) require the assumption that the entire jet expands at the speed of sound. On the other hand, completely ignoring the lateral expansion was found to result in insufficient steepening across the jet break. This scenario seems consistent with our results.

A complication was noted by Gompertz et al. (2018), who find that using different synchrotron relations to estimate $p$ (such as using the spectral index or the pre- or post-break decline) typically results in different estimates, with an intrinsic scatter on the value of $p$ of $0.25 \pm 0.04$ (we will denote this as $\sigma_p$). They argue this is probably caused by emission from GRB afterglows not behaving exactly as the rather simplified analytical models predict.\footnote{We note that the inconsistency between $p$ values derived from the optical and X-ray pre-break slopes assuming a wind-type CBM is $>2\sigma$, so an ISM-like density profile is still favored.} Taking this scatter into account, both $\alpha_{2,\text{FWHM}}$ and $\alpha_{2,\text{AX}}$ in the $\omega = 10$ case (or simply using the only $>26.5$ days points and a single power law) are in fact consistent within $\approx 1\sigma_p$ with $f_\nu \propto t^{-\beta}$. Thus, lateral expansion at the speed of sound can still account for the observed late-

time decline. Using closure relations for both the light curve and the spectrum, Gompertz et al. (2018) found a best fit of $p = 2.06 \pm 0.13$ for GRB 160625B, which is consistent with our results in both bands within $\sigma_p$. In any case, for this burst, some form of lateral expansion is required, and the edge effect alone is insufficient.

We can also attempt to use the results from BOXFIT to determine if the magnetar spin-down power source is consistent with the GRB. The rotational energy that can be extracted from a millisecond magnetar is (Lü & Zhang 2014; Kumar & Zhang 2015)

$$E_{\text{rot}} \approx 2 \times 10^{52} \text{erg} \frac{M}{1.4M_\odot} \left(\frac{R}{10 \text{ km}}\right)^2 \left(\frac{P_0}{1 \text{ ms}}\right)^{-2},$$

where $M$ is the mass, $R$ is the radius, and $P_0$ is the initial spin period of the newborn magnetar. Metzger et al. (2015) placed a limit of $\sim 1 \times 10^{53}$ erg on the maximum energy of a newborn magnetar in extreme circumstances (in terms of mass and spin period). Therefore, the energy requirements of all of the fits from BOXFIT may technically be achievable with the magnetar model, but with the (more realistic) low $\xi$ values, the required energy approaches or exceeds even this maximum limit. The exceptionally high $E_{\text{iso}}$ can be due to a relatively narrow jet and a lower explosion energy instead, but this requires a high $\xi$ that is inconsistent with simulations by Sironi & Spitkovsky (2011) and Warren et al. (2018)—the best fit at $\xi = 1$ also results in an extremely low density more typical of intergalactic environments. We do point out a caveat that the parameters of the best fits show a non-monotonic dependence on $\xi$, with notable degeneracy between parameters.

We have attempted to use BOXFIT to estimate errors for the best-fit parameters as well. However, as a result of what seems to be a bug in the error estimation routine of BOXFIT (G. Ryan and H. van Eerten 2019, private communication), some of the errors are clearly incorrect and, therefore, we have not included errors in our Table 6. This mostly manifests as error limits that either do not include the best fit or where the best-fit value of a parameter is always the lower limit as well.\footnote{In other cases, such as the $\xi = 0.1$ case of GRB 160625B, the errors are seemingly reasonable ($p = 2.05 \pm 0.01$, $E_{\text{iso}} = 1.4_{-0.5}^{+1.3} \times 10^{54}$ erg, $\epsilon_v = 0.2_{-0.13}^{+0.17}$, $\epsilon_b = 3.0_{-2.0}^{+1.6} \times 10^{-4}$, $n = 0.18_{-0.13}^{+0.15}$ cm$^{-3}$, $\theta_h = 0.14 \pm 0.03$ rad, and $\theta_{\text{iso}} = 1.1_{-0.7}^{+1.2} \times 10^{-3}$ rad), and the relative ranges of each parameter are comparable to those found by Alexander et al. (2017). These values thus give an indication of how well each parameter is constrained.} We also note that, as the shape of the radio light curve is not well reproduced in any of our fits, error limits could be misleading in any case. As a consistency check for the rest of the code, we have run BOXFIT using the Alexander et al. (2017) forward shock parameters, which are similar to our $\xi = 1$ results. The output light curves and spectra are similar to the analytical ones and reproduce the early behavior of the afterglow well, although post-break fluxes are somewhat under-predicted.

We also note that the 6.1 GHz light curve of GRB 160625B is not successfully reproduced by BOXFIT, and the jet model struggles to explain the late slope of $\alpha_{6.1\text{GHz}} = -1.08 \pm 0.11$ and the lack of an observed jet break. At low $\xi$ values, the BOXFIT fit is somewhat better but only if one ignores the 22.5 days point, where a low-frequency scattering event by an intervening screen, suggested by Alexander et al. (2017), may contribute to the flux. The radio SED shows a peak centered at 3 GHz between 12 and 22 days, which then disappears. Even...
so, the fit at 22 GHz is worse at all $\xi$ values. At 48 days, the radio SED is consistent with being entirely flat, which is only plausible in the standard model around a very smooth $\nu_m$ break. While the low $\xi$ fits do place the $\nu_m$ passage at roughly this time, the peak in the BOXFIT spectrum is too sharp, and in earlier spectra, the lowest frequencies must then be brightened by a factor of 10 or so by the proposed scattering. The shape may instead be altered by another emission source contributing to the spectrum (see below).

Theoretically expected post-break values in the slow-cooling scenario ($\nu_m < \nu_c$) are $-p$ or $-1/3$, depending on which side of $\nu_m$ the band is located (Rhoads 1999). As the jet break is a geometric effect, we should see it in every band, but this is not the case: we can set a limit of $I_{6.1\text{GHz}} > 10 \times I_{\text{F606W}}$. The possibilities given by the standard jet model that are consistent with the slope are:

1. Post-break, $\nu_c < \nu_m$, i.e., fast-cooling: $\alpha_{6.1\text{GHz}}$ is consistent with the expected decline of $\alpha_2 = -1$. However, the measured $\alpha_{1\text{F606W}} = -0.96 \pm 0.01$ does not match the pre-break decline expected at any frequency in this scenario.

2. Pre-break, $\nu_m < 6.1$ GHz $< \nu_c$: $\alpha_{6.1\text{GHz}}$ is consistent with $p = 2.4$ and $\alpha = 3(1-p)/4 = -1.05$ (Granot & Sari 2002). However, the spectral index between radio and optical is $-0.35 \pm 0.03$ at 22 days and $-0.49 \pm 0.01$ at 140 days, which is intermediate between the indices expected above and below $\nu_m$ (respectively, $(1-p)/2 \approx -0.65$ and $1/3$) and, thus, implies that $\nu_m > 6.1$ GHz at 140 days, or that $p \approx 2.0$.

3. A transition to a nonrelativistic flow, $\nu_m < 6.1$ GHz $< \nu_c$: the expected slope is $(21-15p)/10$ (van der Horst 2007), resulting in $p = 2.12 \pm 0.08$, which is consistent with our estimate within $\sigma_p$. However, such a transition is not seen in the optical or X-ray bands.

The LGRB population has been observed to be comprised of a radio-quiet and a radio-loud population, where the radio-quiet GRBs are incompatible with a simple sensitivity effect and a radio-quiet and a radio-loud population, where the radio-quiet GRBs to have radio fluxes unambiguously too high for the standard model, which, to our knowledge, has not been seen.

One explanation for the “extra” radio source, with its lack of a jet break and the requirement of $6.1$ GHz > $\nu_m$, could be a two-component jet, where a narrow jet core is surrounded by a cocoon with a lower Lorentz factor (Berger et al. 2003; Peng et al. 2005), resulting in a different source with different physical parameters dominating the radio emission and, thus, a different break time and $\nu_m$. This does not result in a deficit in radio synchrotron flux, only an inconsistency between the light-curve shape and the standard model. For an on-axis or slightly off-axis burst ($\theta_{\text{obs}} < \theta_{\text{narrow}}$), the wider component would not contribute significantly to the optical light curve if its kinetic energy is lower than that of the narrow component (Peng et al. 2005). This may also affect the required energy, but without robust modeling, it is difficult to say whether the consistency with a magnetar energy source would change.

Strausbaugh et al. (2018) suggested a scenario where a very smooth cooling transition (i.e., not a normal spectral break) is moving through the optical and infrared frequencies, starting at early times, and the optical spectrum becomes consistent with $\nu > \nu_c$ by ~50 days. This would indicate a unique cooling behavior inconsistent with the standard expectations. The observed lack of evolution of the Swift spectra until 30 days implies that the X-ray spectral slope $\beta_X$ is not the result of a $\nu_c$ break right below the X-ray frequencies, as this would require the spectrum to soften over time to its slope at $\nu > \nu_c$. Furthermore, the optical-to-X-ray index is observed to gradually steepen and eventually become similar to $\beta_X$. This is qualitatively consistent with the reddening of the optical spectrum noted by Strausbaugh et al. (2018). In addition, $\beta_X$ indicates a different $\nu$ than the X-ray light curve; this agrees with the implication of Gompertz et al. (2018) that some physics is missing or simplified in the relevant closure relations. Another possible explanation is that a Klein–Nishina correction (Nakar et al. 2009) is needed above $\nu_c$: this can result in $\beta = 3(1-p)/4$, which would imply $p \approx 2.1$. This harder spectrum is expected to dominate when the $e_c/e_B$ ratio is high, which would fit the low-$\xi$ BOXFIT results.

4.2.2. GRB 160509A

In the case of GRB 160509A, the change in X-ray decay slope across the break, $\Delta \alpha_X = -0.75 \pm 0.11$ for a sharp break and $\Delta \alpha_X = -0.92 \pm 0.15$ for a smooth break. Thus, we cannot exclude the $t^{-3/4}$ factor expected from the edge effect alone in an ISM-like medium. The $t^{-1/2}$ factor expected in the case of a wind medium is consistent with the observations at a $2.3\sigma$ or $3\sigma$ level, depending on $\omega$. However, when considering the intrinsic $p$ scatter of $\sigma_p = 0.25$ (Gompertz et al. 2018), $\alpha_{2X}$ is also consistent with an $f_p \propto t^{-p}$ decline. Thus, we cannot say conclusively whether lateral expansion is important in the jet of GRB 160509A, but it does not seem necessary. In the IR, the measured slope of $\alpha_{2F160W} = 2.09 \pm 0.10$ is marginally consistent (1.1$\sigma$) with $p \approx 2.2$, but a lack of pre-break data prevents us from determining $\Delta \alpha_{F160W}$.

The decline of the afterglow in the radio after 10 days is about $f \propto t^{-0.9}$ at both 6 and 9 GHz (and consistent with this at other frequencies where fewer points are available). This is again inconsistent with the expected post-jet-break slope of $-p$.
or $-1/3$ in the slow-cooling case, respectively, above and below the characteristic synchrotron frequency $v_{m}$ (Rhoads 1999). As with GRB 160625B, we list the possibilities consistent with this decline, allowed by standard jet theory:

1. Post-break, $v_{c} < v_{m}$, i.e., fast-cooling: $\alpha = -1$ is expected and consistent with $\epsilon_{\text{radio}}$, but this scenario is incompatible with the measured IR-to-X-ray spectral index $-0.74 \pm 0.09$ at 35 days, as the expected index is $-p/2 \approx -1.1$ (a photon index consistent with this is indeed seen in the X-ray at earlier times according to the UKSSDC Swift Burst Analyzer)\(^{29}\) — $\langle \delta B \rangle = 1.06 \pm 0.04$ between 1 and 10 days, indicating that $v_{c}$ is still between X-ray and optical frequencies and $v_{c} > v_{m}$ at 35 days.

2. Pre-break, $v_{m} < 6$ GHz $< v_{c}$, ISM-like CBM: $\epsilon_{\text{radio}}$ is consistent with the expected decline ($\alpha = 3(1-p)/4 = -0.9$ assuming $p = 2.2$; Granot & Sari 2002), but the observed spectral index of $-0.40 \pm 0.01$ between F160W and 9 GHz at 35 days implies $v_{m} > 9$ GHz.

3. A transition to a nonrelativistic flow, $v_{m} < 6$ GHz $< 9$ GHz $< v_{c}$: the expected slope is $21(\sim 15p)/10$, resulting in $p = 2.01 \pm 0.08$ — again, consistent with our estimate within $\sigma_{p}$. However, such a transition is not seen in the X-ray light curve, which continues to evolve consistently with a relativistic flow.

The best BOXFIT fit at $\xi = 1$ places a smooth and, thus, off-axis, jet-break at a later time, around 35 days in all bands, in which case the radio light curve would include contamination from the reverse shock at early times, changing the decline slope (see Figure 8). This is because BOXFIT attempts to fit a model with a late break to $f_{\nu} \propto \nu^{-p}$ in order to match the radio light curve, which has no observed break. It is incompatible with the broken power-law fit with $t_{\text{f}} \sim 3.5$ days, though, and at lower, more realistic values of $\xi$ the break is placed at an earlier time. This scenario is therefore not supported. Instead, for GRB 160509A, we can place a lower limit of $t_{\text{break,radio}} \gtrsim 20 \times t_{\text{break,X}}$ based on the broken power-law fit. The situation in the radio frequencies is thus qualitatively very similar to that of GRB 160625B, and the same mechanisms may well be in effect.

We note that Kangas & Fruchter (2019) are, in fact, able to get a plausible fit to the GRB 160509A radio light curve using an analytical fit based on the standard model, but only if the light curve smoothly turns over to a $\nu^{-p}$ decline immediately after the last radio epoch, which is suspicious as their sample contains several GRBs with no unambiguously observed radio breaks, and many cases where the standard model does not fit the radio light curve. We also note that as Laskar et al. (2016) showed, the radio SED seems to remain roughly flat after the reverse shock influence on the light curve fades (~20 days), which might again be caused by another emission component. As BOXFIT also disagrees with this analytical model, one or the other is in doubt. The issue will be addressed in more detail in the upcoming revised version of that paper.

A BOXFIT simulation using the FS parameters of the Laskar et al. (2016) analytical model agrees fairly well with the X-ray data and reproduces the rough magnitude of the radio light curve but not its shape (assuming some RS contribution not accounted for by BOXFIT), but it over-predicts the IR flux by a factor of about 10. Their IR light curve does not include host subtraction, and they fit for extinction as another free parameter in their model. Our host subtraction allows us to estimate the extinction and true IR fluxes independently, and in light of this, the Laskar et al. (2016) model becomes incompatible with the IR data. Thus, our BOXFIT results provide a better reproduction of the light curve in the IR. However, again, the fit parameters show a non-monotonic dependence on $\xi$. As with GRB 160625B above, BOXFIT was clearly unable to produce meaningful error bars for the parameters in some cases, and these are not included in Table 8\(^{30}\) — and, as the radio light curve is again problematic for the fit, would be misleading in any case.

Keeping in mind the caveats associated with our best BOXFIT fits, we can use them to estimate the energy requirements. The geometry-corrected jet energy $1.8 \times 10^{52}$ erg at $\xi = -1$ is well below the maximum rotational energy of a millisecond magnetar (see Section 4.2.1) Once again, we deem the lower $\xi$ values to be more realistic based on simulations (Sironi & Spitkovsky 2011; Warren et al. 2018) and the fact that $\xi = 1$ results in an extremely low density. Low $\xi$ values require energies around $\sim 3 \times 10^{52}$ erg, which again strains the magnetar spin-down model but does not rule it out. Thus, GRB 160509A also seems compatible with a magnetar power source.

For both GRBs considered here (Tables 6 and 8), but especially for GRB 160509A, the efficiency $\eta$ of the prompt $\gamma$-ray emission depends on the value of $\xi$ used in the fitting but not monotonically: with $\xi = 0.01$, one obtains a much lower value for $\eta$ than otherwise. In both cases, the difference in $\chi^{2}$ between the $\xi = 0.1$ and $\xi = 0.01$ fits is minimal, and in the case of GRB 160509A, so is the difference between $\xi = 1$ and $\xi = 0.01$; thus, we cannot reliably distinguish between these scenarios. In the literature, it is commonly assumed that $\xi = 1$, and high values of $\eta$ are obtained: for example, Lloyd-Ronning & Zhang (2004) find values as high as $\eta \sim 1$ depending on $E_{\text{iso}}$, and mostly $\eta \gtrsim 0.3$. Such a high efficiency is used as a criterion for successful models of prompt emission, e.g., the internal shock mechanism tends to result in $\eta \lesssim 0.1$ (Kumar & Zhang 2015, and references therein). Our results may indicate

\(^{29}\) http://www.swift.ac.uk/burst_analyser/00020607/

\(^{30}\) Again, the ranges of each parameter at $\xi = 0.1$, which are large but not obviously incorrect, may provide some indication of how well each parameter is constrained: ($p = 2.13_{-0.02}^{+0.01}$, $E_{\text{iso}} = 3.8_{-0.3}^{+0.4} \times 10^{53}$ erg, $\epsilon_{v} = 0.45_{-0.20}^{+0.31}$, $c_{\text{iso}} = 1.7_{-0.0}^{+0.2} \times 10^{5}$, $n = 18_{-18}^{+18} \text{ cm}^{-3}$, $\theta_{c} = 0.20_{-0.18}^{+0.18}$ rad and $\theta_{\text{obs}} = 0.12_{-0.12}^{+0.12}$ rad).
that if very low values of $\xi$ are more realistic (Warren et al. 2018), one should not dismiss models based on low efficiency.

5. Conclusions

We have presented our late-time optical, radio, and X-ray observations of the afterglows of GRB 160625B and GRB 160509A. We have fitted broken power-law functions to the data, combined with light curves from the literature, to constrain the jet break time and the post-jet-break decline, and used the numerical afterglow fitting software BOXFIT (van Eerten et al. 2012) to constrain the physical parameters and energetics of the two bursts. Our conclusions are as follows.

Regardless of the sharpness of the GRB 160625B jet break, we find that the effect of the jet edges becoming visible as the jet decelerates is alone insufficient to explain the post-jet-break light curves. A full lateral expansion break onto a $r^{-n}$ decline is also inconsistent with the favored sharp break. The light-curve behavior seems qualitatively consistent with the edge effect combined with only a fraction of the jet expanding at the speed of sound (van Eerten & MacFadyen 2012). It is also possible that an intrinsic scatter in the electron Lorentz factor distribution index $p$ exists, the result of simplified synchrotron theory and closure relations that do not necessarily reflect the true complexity of the emission region (Gompertz et al. 2018). This scenario combined with lateral expansion is also consistent with our results. For GRB 160509A, we are unable to exclude any of the considered scenarios due to the scarcity of the available data.

Based on the best fits from BOXFIT, the geometry-corrected energy requirements of both GRBs are consistent with a magnetar spin-down energy source—albeit only in extreme cases when the “participation fraction” (fraction of electrons accelerated into a nonthermal distribution) is fixed at $\xi = 0.1$ or $\xi = 0.01$, requiring energies of $\sim 3 \times 10^{52}$ or even $\sim 10^{53}$ erg. As simulations have shown these lower fractions to be more realistic (e.g., Warren et al. 2018), it seems that magnetar spin-down alone struggles to produce the required energies unless the nascent magnetar has extreme properties (Metzger et al. 2015).

However, neither BOXFIT nor analytical relations from standard jet theory (e.g., Rhoads 1999; Granot & Sari 2002) can provide a good fit to the radio data of either GRB, which are consistent with a single power law that requires the jet break to occur much later in radio than in the other bands. Both GRBs also show an almost flat radio SED at relatively late times (tens of days; see Laskar et al. 2016; Alexander et al. 2017). The higher frequencies do conform to expectations from the jet model, though. This might be the result of a multicomponent jet, but that would require the wide component of the jet to dominate the light curve and simultaneously suppressed flux from the narrow component. A similar behavior (a radio decline described by a single power law with $\alpha = -1.19 \pm 0.06$ until $\sim 60$ days) was recently reported for GRB 171010A by Bright et al. (2019). We explore this problem further in a companion paper (Kangas & Fruchter 2019) and find that these GRBs are not exceptional in this regard.

We thank the anonymous referee for comments that improved the paper. We also thank Hendrik van Eerten, Geoffrey Ryan, Alexander van der Horst, Paz Beniamini, and Chryssa Kouveliotou for helpful discussions.

A.C. acknowledges support from the National Science Foundation via CAREER award #1455090. A.d.U.P. acknowledges support from a Ramon y Cajal fellowship (RYC-2012-09975), from the Spanish research project AYA2017-89384-P, and from the State Agency for Research of the Spanish MCIU through the “Center of Excellence Severo Ochoa” award for the Instituto de Astrofísica de Andalucía (SEV-2017-0709). A.P. wishes to acknowledge support by the European Research Council via the ERC consolidating grant #773062 (acronym O.M.J.). A.C. acknowledges the support of NASA MlRO grant NNX15AP95A.

Based on observations made with the NASA/ESA Hubble Space Telescope (programme GO 14353, PI Fruchter), obtained through the data archive at the Space Telescope Science Institute (STScI). STScI is operated by the Association of Universities for Research in Astronomy, Inc. under NASA contract NAS 5-26555. Support for this work was also provided by the National Aeronautics and Space Administration through Chandra Award Number 17500753, PI Fruchter, issued by the Chandra X-ray Center, which is operated by the Smithsonian Astrophysical Observatory for and on behalf of the National Aeronautics Space Administration under contract NAS8-03060.

This work made use of data supplied by the UK Swift Science Data Centre at the University of Leicester as well as observations made with the Gran Telescopio Canarias (GTC), installed in the Spanish Observatorio del Roque de los Muchachos of the Instituto de Astrofísica de Canarias, in the island of La Palma. Development of CIRCE was supported by the University of Florida and the National Science Foundation (grant AST-0352664), in collaboration with IUCAA.

The National Radio Astronomy Observatory is a facility of the National Science Foundation operated under cooperative agreement by Associated Universities, Inc.

Development of the BOXFIT code was supported in part by NASA through grant NNX10AF62G issued through the Astrophysics Theory Program and by the NSF through grant AST-1009863. Simulations for BOXFIT version 2 have been carried out in part on the computing facilities of the Computational Center for Particle and Astrophysics (C2PAP) of the research cooperation “Excellence Cluster Universe” in Garching, Germany.

Facilities: HST(WFC3), Chandra(ACIS-S), VLA, GTC (CIRCE).

Software: DRIZZLEPAC (Hack et al. 2013); PYRAF (Science Software Branch at STScI 2012); IRAF (Tody 1986); CIAO (Fruscione et al. 2006); CASA (McMullin et al. 2007); ISIS (Alard & Lupton 1998; Alard 2000); BOXFIT (van Eerten et al. 2012).

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