Observational signatures of past mass-exchange episodes in massive binaries: The case of HD 149 404$^{*}$,$^{**}$

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Received 12 October 2015 / Accepted 14 January 2016

ABSTRACT

Context. Mass and momentum exchanges in close massive binaries play an important role in their evolution, and produce several observational signatures such as asynchronous rotation and altered chemical compositions, that remain after the stars detach again.

Aims. We investigated these effects for the detached massive O-star binary HD 149 404 (O7.5f + ON9.7i, P = 9.81 days), which is thought to have experienced a past episode of case A Roche-lobe overflow (RLOF).

Methods. Using phase-resolved spectroscopy, we performed the disentangling of the optical spectra of the two stars. The reconstructed primary and secondary spectra were then analysed with the CMFGEN model atmosphere code to determine stellar parameters, such as the effective temperatures and surface gravities, and to constrain the chemical composition of the components. We complemented the optical study with the study of IUE spectra, which we compare to the synthetic binary spectra. The properties of the stars were compared to evolutionary models.

Results. We confirmed a strong overabundance in nitrogen ([N/C] $\sim$ 150[N/C]$_{\odot}$) for the secondary and a slight nitrogen over-abundance ([N/C] $\sim$ 5[N/C]$_{\odot}$) for the primary star. Comparing the two stars, we found evidence for asynchronous rotation, with a rotational period ratio of 0.50 ± 0.11.

Conclusions. The hypothesis of a past case A RLOF interaction in HD 149 404 is most plausible to explain its chemical abundances and rotational asynchronicity. Some of the observed properties, such as the abundance pattern, are clearly a challenge for current case A binary evolution models, however.

Key words. stars: early-type – stars: fundamental parameters – binaries: spectroscopic – stars: individual: HD 149 404 – stars: massive

1. Introduction

As shown in recent studies (e.g. Sana et al. 2012), a large portion of massive stars belongs to binary or higher multiplicity systems. Whilst this multiplicity permits observationally determining the minimum masses of the stars through their orbital motion, it also leads to complications. For instance, the binnarity of massive stars can result in interactions between their stellar winds that produce observational signatures throughout the electromagnetic spectrum (e.g. Rauw 2013). Moreover, during the lifetime of a massive binary, the binnarity influences the evolution of the stars in various ways (e.g. Langer 2012). These evolutionary effects range from tidally induced rotational mixing (e.g. de Mink et al. 2009) over exchange of matter and angular momentum through a Roche lobe overflow (RLOF) interaction (e.g. Podsiajowski et al. 1992; de Loore & Vanbeveren 1994; Wellstein et al. 2001; Hurley et al. 2002) to the merging of both stars (e.g. Podsiajowski et al. 1992; Wellstein et al. 2001). In RLOF interactions, three different situations are distinguished: case A, for which the RLOF episode occurs when the mass-donor is on the core-hydrogen burning main-sequence; case B, when the star is in the hydrogen-shell burning phase; and case C, for which the star is in the helium-shell burning phase (Kippenhahn & Weigert 1967; Vanbeveren et al. 1998). These binary interactions significantly affect the physical properties of the components and their subsequent evolution. Despite considerable progresses in theoretical models, there remain a number of open questions such as the actual efficiency of accretion (e.g. Wellstein et al. 2001; de Mink et al. 2007; Dray & Tout 2007). To better understand this phenomenon, we need in-depth studies of systems undergoing or having undergone mass exchange.

In this context, HD 149 404 is an interesting target. It is a detached, non-eclipsing O-star binary, member of the Ara OB1 association, located at a distance of 1.3 ± 0.1 kpc (Herbst & Havlen 1977). The orbital parameters were revised by Rauw et al. (2001). These authors found an orbital period of 9.81 days and a circular orbit. They also estimated an orbital inclination of 21° by comparing “typical” masses of supergiants with similar spectral types to those of both components. The spectrum of HD 149 404 displays variable emission lines ([He II] $\lambda$ 4686, [H$\alpha$] that are likely indicative of a wind-wind interaction (Rauw et al. 2001; Thaller et al. 2001; Nazé et al. 2002). One of its components was assigned an ON spectral type, which suggests a significant nitrogen enrichment of its atmosphere.

In this study, we determine the fundamental parameters of the stars of this system through several analysis techniques. The data used in our study are presented in Sect. 2. In Sect. 3

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$^*$ Based on observations collected at the European Southern Observatory (La Silla, Chile) and with the International Ultraviolet Explorer.

$^{**}$ The reduced spectra are only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/A+A/588/A10

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we present the preparatory treatment of our data, which included disentangling the spectra of the binary system to reconstruct individual spectra of the binary components, which are needed for the subsequent spectral analysis. The spectral analyses were made with the non-LTE model atmosphere code CMFGEN and are presented in Sect. 4. In Sect. 5 we discuss the evolutionary state of HD 149 404 and compare it with similar systems.

2. Observational data

The optical spectra analysed here are the échelle spectra used by Rauw et al. (2001) in their study of the orbital solution and wind interactions of HD 149 404. These data were collected in May 1999 and February 2000 with the FEROS and Coralie spectrographs mounted on the ESO 1.5 m telescope and 1.2 m Euler Swiss telescope at La Silla, respectively. The FEROS and Coralie spectrographs have resolving powers of 48 000 and 50 000 and cover the wavelength ranges 3650–9200 Å and 3875–6800 Å, respectively. Further details on the instrumentation and the data reduction are given by Rauw et al. (2001). Because of some problems with the extraction of the FEROS data of May 2000, the normalization of the latter was more uncertain, and we therefore excluded these data from the disentangling procedure, and thus from the further analysis.

To complement our optical data, we also retrieved 25 short-wavelength, high-resolution (SWP) IUE spectra of HD 149 404 from the IUE archives. These spectra were previously described by Stickland & Koch (1996).

Table 1 yields the journal of observations along with the orbital phases computed according to the ephemerides of Rauw et al. (2001), their He I 4471 orbital solution. The optical spectra provide a good sampling of the orbital cycle, which is important for the disentangling in Sect. 3.

3. Preparatory analysis

3.1. Spectral disentangling

The previous determination of the orbital solution of the system performed by Rauw et al. (2001) allowed us to recover the individual spectra of both components by separating the normalized spectra of the binary system. For this purpose, we used our disentangling routine (Rauw 2007), which is based on the method of González & Levato (2006) and was previously used by Linder et al. (2008) and improved by Mahy et al. (2012). The basic idea behind this technique is that the most natural way to handle spectra for radial velocity measurements is to express them as a function of \( x = \ln \lambda \) instead of as a function of \( \lambda \). In this way, the Doppler shift for a line of rest wavelength \( \lambda_0 \) can be expressed as

\[
\ln \lambda = \ln \left[ \lambda_0 \left(1 + \frac{v}{c}\right) \right] = \ln \lambda_0 + \ln \left(1 + \frac{v}{c}\right) \\
= \ln \lambda_0 + \frac{v}{c} \\
\Rightarrow x = 0 + \frac{v}{c}.
\]

Let \( A(x) \) and \( B(x) \) be the spectra of the primary and secondary in the heliocentric frame of reference. In the absence of line profile variability and eclipses, the spectrum observed at any phase \( \phi \) can be written as

\[
S(x) = A \left( x - \frac{v_A(\phi)}{c} \right) + B \left( x - \frac{v_B(\phi)}{c} \right).
\]

| Optical spectroscopy | HDJ-2 440 000 | Inst. | JD-2 440 000 | \( \phi \) |
|----------------------|--------------|-------|-------------|-------|
| 1299.796             | FEROS        | 0.24  |
| 1300.788             | FEROS        | 0.34  |
| 1301.792             | FEROS        | 0.45  |
| 1302.783             | FEROS        | 0.55  |
| 1304.792             | FEROS        | 0.75  |
| 1307.856             | Coralie      | 0.68  |
| 1309.879             | Coralie      | 0.78  |
| 1308.872             | Coralie      | 0.88  |
| 1311.864             | Coralie      | 0.98  |
| 1312.869             | Coralie      | 0.90  |
| 1313.877             | Coralie      | 0.19  |
| 1314.857             | Coralie      | 0.29  |
| 1315.845             | Coralie      | 0.39  |
| 1316.870             | Coralie      | 0.49  |
| 1317.861             | Coralie      | 0.59  |
| 1318.886             | Coralie      | 0.70  |
| 1319.886             | Coralie      | 0.90  |

Table 1. Journal of the optical (top) and UV (bottom) spectra.

where \( v_A(\phi) \) and \( v_B(\phi) \) are the radial velocities of stars A and B at orbital phase \( \phi \).

For a total of \( n \) observed spectra, the spectrum of the primary can be computed as the average of the observed spectra from which the secondary spectrum shifted by the appropriate radial velocity (RV) has been subtracted (González & Levato 2006):

\[
A(x) = \frac{1}{n} \sum_{i=1}^{n} \left[ S_i \left( x + \frac{v_A(\phi_i)}{c} \right) - B \left( x - \frac{v_B(\phi_i)}{c} - \frac{v_A(\phi_i)}{c} \right) \right].
\]

And similarly for the secondary:

\[
B(x) = \frac{1}{n} \sum_{i=1}^{n} \left[ S_i \left( x + \frac{v_B(\phi_i)}{c} \right) - A \left( x - \frac{v_A(\phi_i)}{c} - \frac{v_B(\phi_i)}{c} \right) \right].
\]

Starting from an initial approximation for \( B(x) \) (a flat spectrum), \( v_A(\phi_i) \) and \( v_B(\phi_i) \), we then iteratively determined the primary and secondary spectra and their radial velocities (see González & Levato 2006). For the separations we performed here, we fixed the radial velocities of the binary components to those corresponding to the orbital solution of Rauw et al. (2001).

As for any disentangling method, this technique also has its limitations (González & Levato 2006). A reasonable observational sampling of the orbital cycle is needed because the quality of the results depends on the radial velocity (RV) ranges covered by these observations. Another important limitation is that broad spectral features are not recovered with the same accuracy as narrow ones. This is the case for the wings of the Balmer series.
Table 2. Brightness ratio determination from the dilution of prominent lines.

| Line     | Equivalent width (Å) | Observations | Synthetic spectra | Conti (1973, 1974) |
|----------|----------------------|---------------|-------------------|-------------------|
|          |                      | Primary       | Secondary         | O7.5  | O9.7  | O7.5  | O9.5  |
| He I λ4026 | 0.19                | 0.34          | 0.72              | 0.74   | 0.65  | 0.80  | 0.57  |
| Si IV λ4089 | 0.12                | 0.34          | 0.52              | 0.56   | 0.25  | 0.53  | 0.61  |
| Si IV λ4416 | 0.06                | 0.24          | 0.11              | 0.29   | 0.12  | 0.37  | 0.66  |
| He II λ4200 | 0.11                | 0.08          | 0.47              | 0.21   | 0.42  | 0.23  | 0.61  |
| Hγ       | 0.45                | 0.50          | 1.77              | 1.74   | 1.88  | 2.09  | 0.88  |
| He I λ4471 | 0.17                | 0.37          | 0.55              | 0.69   | 0.71  | 0.97  | 0.58  |
| He II λ4542 | 0.17                | 0.07          | 0.53              | 0.21   | 0.64  | 0.25  | 0.96  |

Notes. The measured EWs are compared with values for the same lines in synthetic spectra of the same spectral type and in the compilation of measurements from the literature. The last column yields the brightness ratio for each line considered, using the synthetic spectra EWs.

3.3. Brightness ratio

Spectral disentangling yields the strength of the lines in the primary and secondary stars relative to the combined continuum, but does not allow establishing the relative strengths of the continua. To further analyse the separated spectra, we therefore need to first establish the brightness ratio of the stars.

To estimate the optical brightness ratio of the components of HD 149 404, we measured the equivalent widths of a number of spectral lines on the separated spectra of the primary and secondary, but referring to the combined continuum of the two stars. The results are listed in Table 2 along with the mean equivalent widths of the same lines in synthetic spectra of stars of the same spectral type, computed with the non-LTE model atmosphere code CMFGEN (Hillier & Miller 1998), which we describe in Sect. 4.2. For comparison, we also list the mean equivalent widths of the same lines in spectra of stars of the same spectral type as evaluated from the measurements of Conti (1973, 1974) and Conti & Alschuler (1971).

The brightness ratio of the two stars can then be evaluated from

\[ \frac{l_1}{l_2} = \frac{EW_{1 \text{obs}}}{EW_{1 \text{mean}}} = \frac{EW_{0.97}}{EW_{0.75}}. \]

By combining our measurements with those from synthetic spectra, we derive an optical brightness ratio of 0.70 ± 0.12 in this way, which is slightly lower than the value found by Rauw et al. (2001), who inferred 0.90 ± 0.16. As a consistency check, we also determined the brightness ratio by comparison with Conti’s measurements and obtained 0.79 ± 0.13. The difference between the results obtained based on synthetic spectra versus Conti’s measurements arises at least partially because Conti (1973, 1974) did not take into account the spectral type O9.7, but instead considered an O9.5 spectral type, consisting of both classes of stars currently known as O9.5 and O9.7.

Reed (2003) reported a mean V magnitude of 5.48 ± 0.02 and B − V colour of 0.39 ± 0.02 for the system. Since the intrinsic \((B − V)_0\) of an O7.5 or O9.5 star is −0.26 (Martins & Plez 2006), the extinction \(A_V\) can be calculated as being 2.02 ± 0.06, assuming \(R_V = 3.1\). Assuming the 1.3 ± 0.1 kpc distance (Wolk et al. 2008), we infer an absolute \(M_V\) of −7.11 ± 0.07 for the binary. A brightness ratio of \(l_1/l_2\) = 0.70±0.12 then yields individual absolute magnitudes of \(M^*_V = −6.15±0.13\) and \(M^*_V = −6.53±0.10\).

The separated continuum-normalized primary and secondary optical spectra are shown and analysed in Fig. 1, in Sect. 4.4.
Table 3. Projected rotational velocities ($v \sin i$ in km s$^{-1}$) of the components of HD 149 404.

| Line         | Primary | Secondary |
|--------------|---------|-----------|
| He I λ4026  | 97      | 75        |
| He I λ4922  | 94      | 64        |
| He I λ5016  | 105     | 58        |
| O III λ5592 | 87      | 55        |
| C IV λ5812  | 82      | 8         |

Mean value = 93 ± 8 km s$^{-1}$

4. Spectral analysis

4.1. Rotational velocities and macroturbulence

After applying a Fourier transform method (Simón-Díaz & Herrero, 2007; Gray, 2008) to the profiles of the He I λ4026, 4922, 5016, O III λ5592, and C IV λ 5812 lines of the separated spectra, we determined the projected rotational velocities $v \sin i$ of the stars of the system. We selected these lines because they are very well isolated in the spectra and are therefore expected to be free of blends. The results are presented in Table 3. The mean $v \sin i$ of the primary star is $(93 \pm 8)$ km s$^{-1}$, while that of the secondary is $(63 \pm 8)$ km s$^{-1}$.

Macroturbulence is defined as a non-thermal motion in the stellar atmosphere in which the size of the turbulent cell is greater than the mean free-path of the photons. The main effect of the macroturbulence is an additional broadening of the spectral lines. This effect has received much attention over recent years (e.g. Simón-Díaz & Herrero, 2014). A first approximation of the macroturbulence velocities is obtained by applying the radial-tangential anisotropic macroturbulent broadening formulation of Gray (2008) on the spectra after including rotational velocity broadening. We used the auxiliary program MACTURB of the stellar spectral synthesis program SPECTRUM v2.76 developed by Gray (2010). We applied this technique to the lines He I λ4026, 4471, and 5016, and He II λ 4542. In this way, we obtained macroturbulence velocities of 70 and 80 km s$^{-1}$ for the primary and secondary stars, respectively. Although this is quite high, these numbers are consistent with measurements of Simón-Díaz & Herrero (2014) that were made on stars of similar spectral types.

Both rotational and macroturbulence velocities were applied on the synthetic spectra (see Sect. 4.2) before comparing the latter with the separated spectra.

4.2. CMFGEN code

To determine the fundamental properties of the components of HD 149 404, we used the non-LTE model atmosphere code CMFGEN (Hillier & Miller, 1998). This code solves the equations of radiative transfer and statistical equilibrium in the co-moving frame for plane-parallel or spherical geometries for Wolf-Rayet stars, O stars, luminous blue variables, and supergiants. CMFGEN furthermore accounts for line blanketing and its effect on the energy distribution. The hydrodynamical structure of the stellar atmosphere is specified as an input to CMFGEN. For the stellar wind, a β wind velocity law. The radiative transfer equations are solved based on the structure of the atmosphere, with a microturbulent velocity varying linearly with velocity from 10 km s$^{-1}$ in the photosphere to 0.1 $v_{\infty}$ at the outer boundary, and generated synthetic spectra are compared to the separated spectra.

As a first approximation, we assumed that gravity, stellar mass, radius, and luminosity are either assumed equal to typical values of stars of the same spectral type (Martins et al., 2005) or adopted from the study of Rauw et al. (2001). The mass-loss rates and β parameters were taken from Muijres et al. (2012) for the spectral types of both stars, whilst the wind terminal velocity was set equal to 2450 km s$^{-1}$ (Howarth et al., 1997) for the two components.

The relevant parameters were then adjusted by an iterative process because each adjustment of a given parameter leads to some modifications in the value of others. This process and the results we obtained are presented in Sects. 4.3 and 4.4.

4.3. Method

The first step was to adjust the temperature in the stellar models. The temperatures were mostly determined through the relative strengths of the He I λ4471 and He II λ 4542 lines (Martins, 2011). The final values are 34 000 and 28 000 K for the primary and secondary stars. Both results agree reasonably well with the temperatures expected for supergiants of these spectral types (Martins et al., 2005).

Subsequently, the natural steps to follow would be adjusting the surface gravities, the mass-loss rate, and the clumping factor, but the binarity of the studied system causes some problems. Indeed, since the wings of broad lines are not properly restored by the disentangling, it is impossible to use the Balmer lines to constrain the surface gravity. And since the Hα and Hβ lines are in addition strongly affected by extra emission from the wind-wind interaction (Rauw et al., 2001; Thaller et al., 2001; Nazé et al., 2002), they cannot be used as diagnostics of the mass-loss rate and clumping factor. The mass-loss rates were therefore fixed to the values tabulated by Muijres et al. (2012) for stars of the same spectral type (see their Table 1, method A). The clumping formalism used in the CMFGEN model is

$$f(r) = f_1 + (1 - f_1)e^{-\frac{r}{r_f}}$$

with a filling factor $f_1$ of 0.1, a clumping velocity factor $f_2$ of 100 km s$^{-1}$, and $V(r)$ the velocity of the wind.

We used an iterative process to constrain the luminosities and surface gravities. The first estimate of $\log(g)$ was taken from Martins et al. (2005) following the spectral types of the stars. Combined with our determination of the effective temperatures, we then inferred the bolometric corrections (Lanz & Hubeny, 2003). This in turn yielded the individual bolometric luminosities, using the absolute $V$ magnitudes of the components derived in Sect. 3.3.

These bolometric luminosities and the effective temperatures were used to compute the ratio of the stellar radii $R_*/M$. Together with the assumed gravities, this ratio yields the spectroscopic mass ratio $M_*/M_1$, which was then compared to the dynamical mass ratio inferred from the orbital solution (Rauw et al., 2001). The difference in these mass ratios was used to produce a new estimate of the surface gravities, and this iterative process was repeated until the spectroscopic and dynamical mass ratios agreed with each other and the CMFGEN synthetic spectra produced for the new gravity values matched the observations as well as possible.
After the fundamental stellar parameters were established or fixed, we investigated the CNO abundances through the strengths of the associated lines. We performed a normalized χ² analysis to determine the best fit to selected lines (Martins et al. 2015). The normalization consists in dividing the χ² by its value at minimum, χ²_min. As a 1σ uncertainty on the abundances, we then considered abundances up to a χ² of 2.0, that is, an approximation for 1 over χ²_min, as suggested by Martins et al. (2015). We used the CIII λλ 4068-70, CII λ 4267, CIII λ 5826, NIII λ 4004, NIII λλ 4511-15-18-24, NII λ 5026, OIII λ 5508, and OIII λ 5592 lines to adjust the C, N, and O abundances of the primary star. For the secondary star, the same lines were used for the N and O abundances, but the only line used for the C abundance was CIII λλ 4068-70. Two methods were used to determine the χ² of each line. First, we compared the depth of the observed and synthetic line cores in the calculation. Second, we determined the mean χ² for every independent point of the full profile of each considered line. The two methods gave similar results. After testing the influence of the errors on projected rotational velocities on the determination of the surface abundances, we found that their effect was small compared to the 1σ uncertainties on the measured abundances as determined here above. We therefore neglected them.

4.4. Results

Figure 1 illustrates the best fit of the optical spectra of the primary and secondary stars obtained with CMFGEN. In Table 4 we present the stellar parameters determined compared to those derived by Rauw et al. (2001). In general, these two works agree well. Table 5 compares the chemical abundances of these best-fit models with solar abundances taken from Asplund et al. (2009).

Figure 1 shows that the He lines and the CIII λλ 4068-70 lines are very well reproduced for both stars. The CIII λ 5696 line cannot be considered in the determination of the surface C abundance since its formation process depends on a number of fine details of atomic physics and of the modelling (Martins & Hillier 2012). Most of the N lines also are very well adjusted. The NII emission lines around 5000 Å in the primary spectrum may be due to emission in the interaction zone, as they are well present in the observed spectrum and not represented in the modelled spectrum. The case of oxygen is more problematic. Whilst OIII λ 5508 is well adjusted, several other OIII lines are present in the synthetic CMFGEN spectra (e.g. OIII λλ 4368, 4396, 4448, 4454, and 4458), but they are barely visible in the separated spectra. We checked that these lines are also absent from the original observed binary spectra. Their absence is thus by no means an artefact that is due to the treatment of our data.
Table 4. Stellar parameters of the primary and secondary stars as obtained with CMFGEN.

|          | This study          | Rauw et al. (2001)     |
|----------|---------------------|------------------------|
|          | Prim.   | Sec.   | Prim.   | Sec.   |
| \( R (R_\odot) \) | 19.3 ± 2.2 | 25.9 ± 3.4 | 24.3 ± 0.7 | 28.1 ± 0.7 |
| \( M (M_\odot) \) | 50.5 ± 20.1 | 31.9 ± 9.5 | 54.8 ± 4.6 | 33.0 ± 2.8 |
| \( T_{\text{eff}} \) \( (10^4 \text{ K}) \) | 3.40 ± 0.15 | 2.80 ± 0.15 | 3.51 ± 0.1 | 3.05 ± 0.04 |
| \( \log (I/I_\odot) \) | 5.63 ± 0.05 | 5.58 ± 0.04 | 5.90 ± 0.08 | 5.78 ± 0.08 |
| \( \log g \) \((\text{cgs})\) | 3.55 ± 0.15 | 3.05 ± 0.15 | 3.05 ± 0.15 | 3.05 ± 0.15 |
| \( \beta \) / \( \text{km s}^{-1} \) | 1.03/1.08 | 1.03/1.08 | 1.03/1.08 | 1.03/1.08 |
| \( \nu_{\text{mic}} \) \((\text{km s}^{-1})\) | 2450/2450 | 2450/2450 | 2450/2450 | 2450/2450 |
| \( M (M_\odot \text{yr}^{-1}) \) | 9.2 × 10^{-7}/ | 3.3 × 10^{-7}/ | 9.2 × 10^{-7}/ | 3.3 × 10^{-7}/ |
| BC       | −3.17   | −2.67   | −3.17   | −2.67   |

Notes. The best-fit CMFGEN model parameters are compared with the parameters obtained by Rauw et al. (2001) for an orbital inclination of 21°. The effective temperatures from Rauw et al. (2001) were derived through the effective temperature calibration of Chlebowski & Garmany (1991) and permitted, along with the determined luminosities, inferring the stellar radii. The quoted errors correspond to 1σ uncertainties. The symbol \( / \) in the table corresponds to values fixed from the literature (Howarth et al. 1997; Muirres et al. 2012). The bolometric corrections are taken from Lanz & Hubeny (2003), based on our best-fit \( T_{\text{eff}} \) and \( \log g \).

Table 5. Chemical abundances of the components of HD 149 404.

|          | Primary   | Secondary  | Sun       |
|----------|-----------|------------|-----------|
| He/H     | 0.10 ± 0.11 | 0.10 ± 0.11 | 0.10 ± 0.11 |
| C/H      | 1.02 ± 0.63 | 1.90 ± 0.47 | 1.89 ± 0.47 |
| N/H      | 1.32 ± 1.10 | 7.15 ± 1.36 | 7.15 ± 1.36 |
| O/H      | 7.33 ± 2.56 | 7.85 ± 2.56 | 7.85 ± 2.56 |

Notes. Abundances are given by number as obtained with CMFGEN. The solar abundances (Asplund et al. 2009) are quoted in the last column. The 1σ uncertainty on the abundances was set to abundances corresponding to a \( \chi^2 \) of 2.0. As only one line was considered for the C abundance of the secondary, the corresponding calculated uncertainty was unrealistically low. A similar problem was encountered for the O abundance of the primary star, for which we only had two lines to work with and several absent lines over the spectrum, as specified in the second paragraph of this section. To circumvent these problems, we set the uncertainties for these two abundances to values close to those calculated for the other two elements of the corresponding star.

We stress two interesting results from our spectral analysis. First of all, we confirm the large overabundance of N in the secondary spectrum. Second, we infer an asynchronous rotation of the two stars. The radii determined with CMFGEN (Table 4), the mean projected rotational velocities (Table 1), and the inclination estimate from Rauw et al. (2001) yield the rotation periods of the primary and secondary stars: 3.77 ± 0.32 days and 7.46 ± 0.95 days, respectively, or a period ratio of 0.50 ± 0.11. We note that within the uncertainties on the inclination, the secondary rotational period is similar to the orbital period of the system (9.81 days). We return to these points in Sect. 5. Finally, we note that according to the radii determined here, none of the stars currently fills its Roche lobe. With the formula of Eggleton (1983), we estimate a Roche-lobe volume filling factor of 15% for the primary and 73% for the secondary.

As pointed out above, disentangling the IUE spectra of HD 149 404 was more problematic, especially for those parts of the UV spectra that feature strong and broad wind lines and/or are polluted by blends with numerous interstellar features. The left panel of Fig. 2 illustrates the comparison of the separated spectra and the synthetic spectra obtained with CMFGEN over a wavelength range that is relatively free of interstellar lines and mainly hosts photospheric lines. The agreement is clearly quite reasonable.

To check whether our CMFGEN models are also able to correctly reproduce the wind features, we re-combine the synthetic CMFGEN UV spectra of the primary and secondary taking into account the radial velocity shifts at the time of the observations. We did so for several orbital phases. The right panel of Fig. 2 illustrates the result for three selected IUE spectra (SWP03008, JD 2 443 798.965, SWP02755, JD 2 443 776.869, and SWP54350, JD 2 449 817.595), corresponding to conjunction phase 0.00 and quadrature phases 0.75 and 0.25. The synthetic spectrum clearly agrees well with the observation, except for a few narrow absorptions that are due to the interstellar medium, which are not taken into account in our model. This additionally supports our determination of the physical parameters of the system components. Moreover, the concordance between the synthetic and observed UV spectra suggests that the P-Cygni profiles form over parts of the stellar winds that are not significantly affected by the wind-wind interactions, the latter leading to a loss of spherical symmetry of the line formation region.

The fluxed CMFGEN spectra also allow us to estimate the brightness ratio (primary/secondary) in the UV. We find a value of 0.91.2

Furthermore, we found relatively little variability of the P-Cygni profiles over the orbital period. Both observations (lack of strong variability and little effect of wind interaction on the line morphology) are likely due to the low orbital inclination \( (\sim 21°) \) of the system. This inclination implies that the observed spectrum arises mostly at high stellar latitudes, where the wind-wind interaction zone has less influence on the wind structure.

5. Discussion and conclusion

5.1. Evolutionary status

As we have shown in the previous section, the spectra of the components of HD 149 404 display the signatures of some
Fig. 2. Upper left panel: comparison between the separated IUE spectra (black) of the primary and secondary stars around the He II λ 1640 line and the corresponding synthetic spectra (red). The primary spectrum is shifted upwards by 0.5 for clarity. The other three panels display a comparison between the SWP03008 (upper right), SWP54350 (lower left) and SWP02755 (lower right) IUE spectra taken at phases 0.0, 0.25 and 0.75 in black and the synthetic binary spectra obtained through combination of CMFGEN primary and secondary spectra at given phases in red.

Figure 3 compares our inferred N/C and N/O ratios with the predictions for the evolution of single massive stars (Ekström et al. 2012) either without rotation (left panel) or with a rotational velocity of 0.4 × v_{crit} (right panel). This figure clearly shows that for the spectroscopic masses of the primary and secondary stars these models cannot account for the observed CNO abundance patterns. For instance, in the case of models without rotation (left-hand panel of Fig. 3), no chemical enrichment is expected during the main-sequence evolution for stars with mass < 60 M_☉. Only for the M > 60 M_☉ model is the loss of material through stellar wind sufficient to reveal the products of the CNO cycle at the surface before the end of the main-sequence evolution. Adopting instead the rotating models (right-hand panel of Fig. 3), the enrichment of the secondary can only be explained by single-star evolution if we assume at least a star with 60 M_☉, whilst the spectroscopic mass is about a factor two lower. When the surface abundances of a single star of 60 M_☉ initial mass reach the values observed for the secondary of HD 149 404, the current mass of the star is still about 50 M_☉, that is, it is much higher than the mass determined for the secondary star.

The observed CNO abundance pattern is qualitatively much easier to interpret if the present-day secondary star was formerly the more massive component of the binary and transferred mass and angular momentum to the present-day primary in an RLOF episode. During this process, the outer envelope of the secondary was removed, revealing layers of material that were previously inside the convective hydrogen-burning core (Vanbeveren 1982, 2011).

We start by comparing our results with theoretical predictions from the literature. The expectation is that the more mass has been lost by the donor, the deeper the layers that are revealed at the surface and thus the higher the N/C ratio. The predicted CNO abundances for the mass loser after a case B mass-transfer episode are [N/C] = 100 [N/C]_⊙ and [N/O] > 5 [N/O]_⊙ (Vanbeveren 1982). This is indeed close to what we observe in our analysis. Moreover, the RLOF scenario is re-enforced by the values of the primary star abundances. Classical radiative equilibrium evolutionary models predict normal H and He abundances for the mass gainer of an RLOF episode, but an N abundance of two to three times solar (Vanbeveren & de Loore 1994), which agrees with our results.

There are some caveats here, however. First, the results of Vanbeveren (1982) apply to case B mass transfer, whereas HD 149 404 is more likely to have undergone a case A mass exchange (see below). Second, when the outer hydrogen-rich layers are removed, an enrichment of the stellar surface of the mass
helium abundance (\textit{spectrum of the secondary of HD 149 404 can be fit with a solar abundance)} of the secondary before the onset of mass transfer must have always accompanied by an increase of the surface helium abundance similar to the one observed for the secondary. If we consider once more the single-star evolutionary tracks with the He abundance set to solar, however, and there is no hint for our models requiring a He enhancement in any of the stars. Although the predicted relative change of helium surface abundance is usually much smaller than for N, this result is nonetheless surprising, especially in view of the large N overabundance reported by our finding that both stars are currently well inside their Roche lobes.

To illustrate the helium enrichment that might be expected, we consider once more the single-star evolutionary tracks with rotation of Ekström et al. (2012). In these models, a nitrogen surface abundance similar to the one observed for the secondary is always accompanied by an increase of the surface helium abundance to values higher than \( y > 0.35 \) by mass. The fact that the spectrum of the secondary of HD 149 404 can be fit with a solar helium abundance \( y = 0.1 \) suggests that the internal structure of the secondary before the onset of mass transfer must have been different from that expected from single-star evolutionary models. Moreover, the RLOF in HD 149 404 must have come to a (temporary) stop before the full hydrogen-rich envelope of the mass donor was removed. The latter conclusion is also supported by our finding that both stars are currently well inside their Roche lobes.

Given the present-day spectroscopic masses, the secondary must have lost at least 9.3 \( M_\odot \) assuming a fully conservative mass transfer. Conservative RLOF will increase the period of the binary. If we assume a fully conservative mass transfer and apply the formula of Vanbeveren et al. (1998), we find that the orbital period would have increased by 17% at most, the shortest possible initial orbital period being 8.4 days for a mass exchange of 9.3 \( M_\odot \). However, Petrovic et al. (2005) argued that in fast case A RLOF, only about 15–20% of the mass shed by the mass donor is indeed accreted by its companion. If the mass-transfer efficiency is that low, then the secondary must have lost a much larger amount of mass. Such a non-conservative mass transfer can result from the transfer of angular momentum. In fact, the mass gainer can be spun up to critical rotation and will then require additional mass (and angular momentum), leading to a non-conservative mass transfer (e.g. Langer et al. 2003; Vanbeveren 2011; Langer 2012). In the previous section, we noted that the components of the system are apparently not in synchronous rotation. This asynchronicity therefore also suggests the existence of a past mass and angular momentum transfer episode, with a clear spin up of the primary star.

In Fig. 4 we present the positions of the primary and secondary stars in the Hertzsprung-Russell diagram (HRD) (upper panels) and in the \( g - \log T_{\text{eff}} \) diagram (lower panels), along with the evolutionary tracks from Ekström et al. (2012) for the core-hydrogen burning phase of single stars at solar metallicity, both for non-rotating (left panels) and rotating (right panels) stars. This figure again illustrates the failure of single-star evolutionary tracks to account for the properties of the components of HD 149 404. If we consider the models without rotational mixing, the position of the primary star in the HRD is relatively close to the track corresponding to its present-day spectroscopic mass. However, the secondary appears too luminous for its present-day mass compared to these evolutionary tracks. If we compare the stars to the 40% critical rotation case, we find that the primary’s luminosity is below that expected for its present-day spectroscopic mass. Moreover, the secondary lies outside the range covered by tracks in the core-hydrogen burning phase. If we consider the non-rotating case, we see that in the \( g - \log T_{\text{eff}} \) diagram the primary star has a lower effective temperature and a higher surface gravity than expected for a 50 \( M_\odot \) star, whilst the secondary star displays parameters corresponding to stars twice as massive as its present-day spectroscopic mass. For stars rotating at 40% of their critical velocity, we find that both stars would have initial masses of about 30 \( M_\odot \). The primary dynamical mass is about a factor 2 higher, while for the secondary the agreement is good. Finally, in all cases (with and without rotation and for both diagrams), the two components of HD 149 404 are not located on the same isochrone, although they would be expected to have the same age\(^3\).

In a mass-transfer episode, the location of both stars in the HRD after the RLOF strongly depends on the details of the process. For instance, spinning-up the mass gainer can lead to

\(^3\) The age of the Ara OB1 association of which HD 149 404 is a member was estimated in the literature as \( \sim 3 \) Myr (Wolk et al. 2008).
almost complete mixing of the latter. In this situation, models predict that He would be enhanced in the atmosphere of the mass gainer and that the latter would become bluer and overluminous for its mass (Vanbeveren & de Loore 1994). If there is no strong spin-up and the accretion occurs rather slowly and is accompanied by a fast diffusion process, then the location of the gainer in the HRD should be very close to that of a normal star of the same mass and chemical composition (Vanbeveren et al. 1998). The star is rejuvenated, however: it lies on an isochrone that corresponds to a younger age than its actual age. The location of the primary in the HRD suggests that in the present case the second scenario is likely to apply with a very moderate rejuvenation, if any, of the primary. This conclusion is supported by the lack of a strong He enrichment, but it is at odds with the highly non-synchronous rotation of the primary reported above.

5.2. Comparison with other post-RLOF systems

In this section, we briefly compare the properties of HD 149 404 with those of two other O-type binaries, Plaskett’s Star and LZ Cephei, which are probably in a post-case A RLOF evolutionary stage and have been analysed in a way similar to the present work (Linder et al. 2008; Mahy et al. 2011).

Plaskett’s Star (HD 47 129) is an O8 III/1 + O7.5 III binary with an orbital period of 14.4 days, slightly longer than that of HD 149 404, and a mass ratio near unity. Two observational
facts suggest that the initially more massive primary has undergone a case A RLOF episode in the past (Linder et al. 2008). First, the projected rotational velocity of the secondary star is remarkably high (mean value of $272.5 \pm 35.0 \text{ km s}^{-1}$) compared to that of the primary (mean value of $65.7 \pm 6.3 \text{ km s}^{-1}$). This strongly asynchronous rotation likely stems from a spin-up of the secondary star through a recent transfer of angular momentum from the primary star. Second, the primary star displays nitrogen overabundance ($N/Na = 16.6 \pm 5.0$) and carbon depletion ($C/C_\odot = 0.2 \pm 0.1$), as is typical of an advanced evolutionary stage, whilst no such nitrogen enrichment is seen in the secondary spectrum. Given the present-day configuration of HD 47 129, it seems that the transfer of angular momentum and the resulting spin-up of the mass gainer (the secondary in this case) might have prevented accretion of a larger portion of the primary’s mass.

LZ Cephei (HD 209 481) is an O9 III + ON9.7 V binary with a short orbital period of 3.07 days (Kameswara Rao 1972) and a mass ratio (primary/secondary) of 2.53 (Mahy et al. 2011). Both components of LZ Cep almost fill their Roche lobe (Mahy et al. 2011; Palate et al. 2013). Mahy et al. (2011) found that the secondary displays a strong nitrogen enrichment (18 times solar), carbon and oxygen depletion (0.1 times solar), and a high helium content (4 times solar), suggesting a very advanced state of evolution. On the other hand, the primary displays only slightly altered surface abundances consistent with single-star evolution. This suggests that the mass transfer was strongly non-conservative. Mahy et al. (2011) noted a slight asynchronicity of the rotation periods of the order of 10−20%, but concluded that the system is probably on the verge of achieving synchronization. Comparison with single-star evolutionary tracks indicates a similar age discrepancy as we have found here for HD 149 404. The evolutionary masses $(25.3^{+4.5}_{-1.6} M_\odot$ and $18.0^{+2.4}_{-0.7} M_\odot$, for the primary and secondary respectively) are significantly higher than their dynamical masses $(16.9 \pm 1.0$ and $6.7 \pm 1.0 M_\odot$, respectively, Mahy et al. 2011; Palate et al. 2013).

Although our sample is currently too limited to draw firm conclusions, the above comparison reveals several interesting results that are worth studying in more detail with a larger sample. First, we note that in all three systems, the components appear either over- or under-luminous when compared with single-star evolutionary tracks corresponding to their present-day masses. During its initial phases, case A mass transfer occurs on a thermal timescale leading to a very rapid mass exchange. However, the mass transfer subsequently slows down and occurs on a nuclear timescale instead. By the time the mass transfer ends, both stars would therefore be expected to be in thermal equilibrium again. Since all three systems under consideration are in a detached configuration, the stars should thus have settled onto their new post-RLOF evolutionary tracks. The discrepancy between the observed luminosities and those predicted by the single-star evolutionary tracks most likely stems from several effects, such as observational uncertainties, altered chemical compositions (and hence opacities of the stellar material), and a rotational velocity history that differs from that assumed in the single-star models.

Our comparison shows that the degree of asynchronicity in the three post-RLOF systems increases with orbital period (from LZ Cep, over HD 149 404 to HD 47 129). This is most probably due to the higher efficiency of the tidal forcing in shorter period systems, or it might be seen as evidence that momentum transfer has played a larger role in those systems that have a wider present-day orbital separation. This is expected since binary evolution models predict spin-up to be less efficient in closer systems because in such systems the accretion stream directly affects the mass gainer without forming an accretion disk (e.g. Langer 2012). The questions of synchronization and circularization in close binary systems with early-type stars, featuring radiative envelopes and convective cores, have been addressed by Zahn (1975) and Tassoul (1987). Zahn (1975) considered radiative damping of the dynamical tide in the outer layers of the stellar envelopes as the main mechanism for synchronization. The corresponding synchronization timescales strongly depend upon the tidal torque constant $E_2$, which varies by several orders of magnitude during the main-sequence lifetime of the star (Zahn 1977). Siess et al. (2013) provided a parametrization of this parameter as a function of stellar mass and relative age of the star. Assuming that their formalism holds for the masses of the stars considered here and adopting an age of half the main-sequence age of the stars, we estimated the values of $E_2$. We then evaluated the synchronization times following Eq. (4.28) of Zahn (1975) by means of moments of inertia tabulated by Claret & Giménez (1992). The results are $5.6 \times 10^6$ and $1.4 \times 10^7$ years for the primary and secondary stars of HD 149 404, respectively, $4.4 \times 10^7$ and $27.6 \times 10^7$ years for the primary and secondary of Plaskett’s star, and $2.8 \times 10^8$ and $2.5 \times 10^7$ years for the primary and secondary components of LZ Cephei. Tassoul (1987), on the other hand, proposed that the most effective mechanism for synchronization is provided by large-scale hydrodynamic motions in the interiors of the tidally distorted binary components. The resulting timescales are considerably shorter than those estimated following the formalism of Zahn (1975). We estimate synchronization timescales of $2.1 \times 10^7$ and $3.2 \times 10^8$ years for HD 149 404, $7.2 \times 10^7$ and $2.0 \times 10^8$ years for Plaskett’s star, and $1.6 \times 10^7$ and $6.0 \times 10^6$ years for LZ Cep. Regardless of which of the two formalism is most appropriate to describe the evolution of rotation in the systems considered here, we find that, except perhaps for Plaskett’s Star, which has a longer synchronization timescale, the RLOF phase probably must have ended less than a few 10$^7$ years ago.

Another puzzling result is the fact that the post-RLOF mass ratio deviates most from unity for the shortest period system (LZ Cep). Therefore, in this system, the RLOF must have been comparatively more efficient than in the longer period systems. As discussed above, the mass transfer in LZ Cep was most likely highly non-conservative. If the material lost by the system does not carry away angular momentum in addition to the intrinsic orbital angular momentum, such a non-conservative mass loss leads to a widening of the orbital separation $a$ given by

$$\frac{da}{dt} = -\frac{M}{a^2} M$$

where $M < 0$ is the mass-loss rate (Singh & Chaubey 1986; Tout & Hall 1991). Assuming a fully non-conservative mass loss, this would imply that the initial orbital period of LZ Cep must have been shorter than 1.5 days. The duration of the RLOF episode depends on the evolution of the Roche-lobe filling factor of the mass donor. The evolution of the size of the Roche lobe is set by the relative importance of the orbit expansion and the shrinking of the relative size of the mass donor’s Roche lobe. In addition, the evolution of the radius of the mass donor needs to be accounted for (see Tout & Hall 1991). Since massive stars...
with radiative envelopes contract considerably on a dynamical timescale (Tout & Hall 1991) and in view of the current mass-ratio of LZ Cep (Mahy et al. 2011), it seems unlikely that a non-conservative RLOF could be the explanation for a more efficient mass loss. Alternatively, if the material lost by the system carried off additional angular momentum, then the result could be a shrinking of the orbit. In active, low-mass stars, such a situation could arise if the material lost by the donor corotates with the latter under the effect of a magnetic field out to a wide distance (Tout & Hall 1991). However, strong magnetic fields are fairly rare among single massive stars (∼7%), and their incidence appears even lower among massive binaries (Neiner et al. 2015). Hence, this scenario also appears very unlikely in the case of LZ Cep.

Clearly, the above trends call for confirmation by studying a larger sample of post-case A RLOF massive binary systems. We are currently undertaking such studies, and the results will be presented in forthcoming publications.

5.3. Summary and conclusion

We analysed the fundamental properties of the binary system HD 149 404 by means of spectral disentangling and the CMFGEN atmosphere code. Our investigation of this object represents a significant improvement over previous studies because we have obtained the individual spectra of each component. This led to the determination of a number of stellar parameters that were used to constrain the evolutionary status of the system.

We established the existence of a large overabundance in N and a C and O depletion in the secondary star and also found a slight N enhancement in the primary’s spectrum. We showed that these surface abundances cannot be explained by single-star evolutionary models. Furthermore, we inferred an asynchronous rotation of the two stars of the system. These two results indicate a previous mass and angular momentum-exchange phase through a Roche-lobe overflow episode. Given the present status of HD 149 404 as an O+O binary, this mass transfer probably was a case A RLOF. However, dedicated theoretical studies are needed to understand the details of the evolution of this system.

Acknowledgements. The Liège team acknowledges support from the Fonds de Recherche Scientifique (FRS/FNRS) including especially an FRS/FNRS Research Project (T.0100.15), as well as through an ARC grant for Concerted Research Actions financed by the French Community of Belgium (Walloon-Brussels Federation), and an XMM PRODEX contract (Belspo). Anthony Hervé is supported by grant 14-0238SS from GA ÇR.

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