**OPTICS**

**Multioctave supercontinuum generation and frequency conversion based on rotational nonlinearity**

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The field of attosecond science was first enabled by nonlinear compression of intense laser pulses to a duration below two optical cycles. Twenty years later, creating such short pulses still requires state-of-the-art few-cycle laser amplifiers to most efficiently exploit “instantaneous” optical nonlinearities in noble gases for spectral broadening and parametric frequency conversion. Here, we show that nonlinear compression can be much more efficient when driven in molecular gases by pulses substantially longer than a few cycles because of enhanced optical nonlinearity associated with rotational alignment. We use 80-cycle pulses from an industrial-grade laser amplifier to simultaneously drive molecular alignment and supercontinuum generation in a gas-filled capillary, producing more than two octaves of coherent bandwidth and achieving 

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\Delta n(t) \approx n_2 I(t)
\]

To this end, substantial effort has been invested into the development of few-cycle laser amplifiers (13, 14) and two-stage compression schemes (15–17), which mitigate the effects of ionization and plasma generation on the efficiency and compressibility of broad supercontinuum spectra.

Recently, molecular gases (18) have been proposed as an alternative to noble gases for hollow-core fiber (HCF) pulse compressors. For molecular gases, the vibrational and rotational degrees of freedom result in the addition of “delayed” nonlinear responses \( \Delta n_d \) caused by the field-induced alignment and stretching of the molecular bonds (19, 20), as well as four-wave mixing processes associated with Raman transitions (21, 22). In the case of linear molecules, the rotational nonlinearity dominates over the vibrational contribution (23) and has only a minimal impact on the propagation of short pulses (below \( \sim 100 \text{ fs} \)) because of a lack of temporal overlap with the delayed response (24). However, it has been exploited to imprint temporal phase shifts onto a second copropagating pulse, which arrives during a revival of rotational coherence (25, 26). Conversely, long input pulses (hundreds of femtoseconds) experience a prolonged interaction that can coincide with the delayed response duration (27), markedly increasing the magnitude of the induced rotational nonlinearity, as illustrated in Fig. 1. For sufficiently long pulses, the enhanced rotational nonlinearity can also be considered to be nearly instantaneous and can yield a qualitatively similar time-dependent nonlinear response as that of the electronic Kerr nonlinearity. By appropriately choosing the molecular gas according to the input pulse duration, the total nonlinearity can be enhanced more than 10-fold in comparison to an atomic gas with similar nonlinear susceptibility and ionization potential (27).

Here, we suggest a conceptually new approach to few-cycle pulse compression, wherein the input pulse duration is chosen to optimize the delayed contributions to the nonlinearity rather than minimize the ionization. By taking advantage of the much larger rotational contribution to the nonlinear index of refraction of molecules (27) and using relatively long laser pulses for which the rotational nonlinearity can be nearly instantaneous, we achieve a record >45\( \times \) pulse compression in a single stage. We also demonstrate the utility of these pulses for applications in attosecond science by generating a

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coherent XUV supercontinuum spectrum through high-order harmonic generation (HHG). Last, we show that the time scale of the rotational nonlinearity can be used to shift the central frequency of the few-cycle pulses, thereby providing a more-efficient alternative to long-wavelength sources based on parametric amplification (28, 29).

RESULTS
To illustrate how the dynamics of the delayed nonlinearity affect the generated supercontinuum, we calculate the spectrum generated from propagation of laser pulses with various input pulse durations (30 fs to 1 ps) in Ar, N₂, and N₂O (Fig. 2) using a model that incorporates the delayed nonlinearities using a density matrix formalism to obtain the total nonlinear phase shift (30). While argon exhibits symmetric spectral broadening throughout, with a spectral bandwidth that quickly shrinks as the input pulse duration increases, both the molecular gases exhibit markedly different behavior depending on the input pulse duration. Both N₂ and N₂O start with a broad supercontinuum at short input pulse durations, which initially shrinks with increasing pulse duration but is then followed by a

Fig. 1. Nonlinear indices and phase shifts. The nonlinear indices of refraction of Ar, N₂, and N₂O (A to C) are calculated for short (30 fs) and long (280 fs) input pulse durations. Ar and N₂ share similar ionization potentials and instantaneous nonlinear refractive indices. Both atomic and molecular systems exhibit an instantaneous response due to the electronic Kerr nonlinearity, while the delayed rotational response ∆n₁, proportional to the degree of alignment in the molecular ensemble, is present only in the molecular systems. For short input pulses, the effective change in refractive index is approximately the same in Ar and N₂ because only the instantaneous contribution takes effect during the period of interaction, whereas the long pulses see a significantly larger ∆n in N₂. The effect is even more pronounced in N₂O, which was chosen because of its larger polarizability anisotropy and longer rotational period. The latter plays a crucial role because the degree to which the temporal evolution of the refractive index coincides with the intensity envelope (shown in gray for the 280-fs pulse) determines the shape of temporal phase shift and thus the time dependence of the instantaneous frequency (D).

Fig. 2. Pulse duration dependence of spectral broadening. Comparison of the supercontinuum spectra simulated in (A) Ar (6.5 bar), (B) N₂ (6.5 bar), and (C) N₂O (4.4 bar) for different input pulse durations at a fixed intensity of 1 TW/cm² reveals the dynamics associated with ∆n₁. In the molecular gases, longer pulses lead to larger degrees of molecular alignment and therefore enhanced nonlinearity. At the same time, the molecular alignment is delayed with respect to the pulse. The combination of these two effects leads to purely red-shifted supercontinuum spectra for pulse durations of approximately 100 fs in N₂ and 150 fs in N₂O. Further increasing the pulse duration shifts the peak of the alignment to coincide with the trailing edge of the pulse, resulting in more symmetric spectra and optimized spectral bandwidth for pulse durations of approximately 150 fs in N₂ and 280 fs in N₂O. The central frequency of the input laser was 0.29 fs⁻¹ in all cases.
strong red shift and subsequent extension to higher frequencies. The blue-shifted components are initially weak but gradually increase in strength with further increasing input pulse duration. Notably, the supercontinuum spectra generated in N₂ and N₂O with very long pulses remain substantially broader than those generated in Ar because of the enhancement afforded by the large rotational nonlinearity. For the longest pulses considered, molecular alignment approaches the adiabatic condition where ∆n_d and ∆n_i have the same qualitative behavior, yielding symmetric spectra with broader bandwidth than their atomic counterparts.

We experimentally demonstrate coherent supercontinuum generation by propagating 400-µJ, 280-fs pulses with a central wavelength of 1025 nm through a 3.5-m-long capillary fiber filled with Ar, N₂, or N₂O. A diagram of the experimental setup is shown in fig. S1. Pressure-dependent spectra for Ar and N₂ up to 6.2 bar and for N₂O up to 4.4 bar are shown in fig. S2, while the spectra collected at the highest pressures are shown in Fig. 3 (A to C). The measured spectra exhibit extensions to both the short- and long-wavelength sides of the input spectrum and amplitude modulations consistent with the SPM process and with numerical propagation simulations (31) shown in Fig. 3 (D to F). This is unlike typical SPM-broadened spectra, where the generation of frequencies below and above the fundamental frequency occurs at the leading and trailing edges of the pulse, respectively, leading to a symmetric spectrum such as that observed in Ar. Instead, due to the delayed rotational nonlinearity, the zero crossing of the instantaneous frequency shift comes after the pulse's peak (Fig. 1D), leading to the enhanced generation of red-shifted frequencies.

At 6.2 bar, the supercontinuum spectra generated in Ar and N₂ cover 200 and 485 nm, respectively. These correspond to bandwidth-limited pulse durations of 21 fs (six cycles at 1026 nm) and 7.4 fs (two cycles at 1094 nm) for Ar and N₂, respectively. In the case of N₂O, the supercontinuum generated at 4.4 bar covers two optical octaves and supports a bandwidth-limited pulse duration of 2.5 fs, less than one optical cycle at a central wavelength of 1068 nm. Synthesis of such short pulses requires that the phase accumulated...
during propagation can be adequately compensated over the entire bandwidth. We separately demonstrate compression of the supercontinuum spectra generated in N₂ and N₂O to few-cycle durations in two spectral regions using dispersion-compensating mirrors (700 to 1400 nm) (32) and an acousto-optic programmable dispersive filter (1100 to 1800 nm) (33). The few-cycle pulses characterized by frequency-resolved optical gating (FROG), and their corresponding spectra, are shown in Fig. 4. Using dispersive mirrors, we generate 7.0-fs (two cycles at 1068 nm) pulses in 6.5 bar of N₂ and 5.8-fs (1.6 cycles at 1074 nm) pulses in 2.4 bar of N₂O, corresponding to a >45-fold compression. With the dispersive filter, we select a region of the spectrum not covered by our dispersive mirrors and demonstrate compression in the long-wavelength region of the generated supercontinuum to 10.4 fs (2.3 cycles at 1374 nm) in 3.0 bar of N₂O. Last, sub-two-cycle pulses were generated in 1.0 bar of N₂O using the maximum input pulse energy of 400 μJ and used to drive HHG in argon gas, where the observation of an XUV continuum reaching 80 eV (fig. S6) demonstrates the high-quality compression suitable for attosecond pulse generation. Compression efficiencies for all generated few-cycle pulses are summarized in the inset of fig. S1.

**DISCUSSION**

The presented results underscore previously unidentified capabilities associated with the judicious choice of molecular gas media for nonlinear propagation according to the laser pulse parameters. In addition to optimizing the accumulated nonlinear phase for supercontinuum generation, we highlight a mechanism through which the laser’s central frequency can be efficiently red-shifted during spectral broadening. Accordingly, for a given molecular gas, there exists a range of pulse durations that can provide either symmetric or red-shifted spectral broadening. We therefore identify propagation in molecular gases as an efficient platform for both the compression of long laser pulses, potentially yielding few-cycle pulses directly from industrial-grade picosecond lasers (34), and the generation of high-energy, long-wavelength femtosecond pulses in hollow-core fibers (see the Supplementary Materials) (35). Optimistically, the use of larger linear molecules with substantially larger electronic and rotational non-linearities and longer rotational periods (36) could potentially allow nonlinear compression of pulses with durations greater than 10 ps, which can be generated via direct amplification.

**MATERIALS AND METHODS**

**Experimental setup**

The experiments were performed by focusing the output of a Yb:KGW laser amplifier (Light Conversion PHAROS: 1025 nm, 280 fs) with a maximum pulse energy and an average power of 400 μJ and 20 W, respectively, onto the entrance of a stretched hollow-core capillary fiber (few-cycle, Inc.: 3.5-m length, 500-μm inner diameter) filled with Ar, N₂, and N₂O. The focal lens (f = 1 m) was mounted on a linear translation stage, allowing the distance between the lens and the fiber entrance to be varied to optimize the coupling efficiency, thereby mitigating the effects of different self-focusing lengths for the different gases. The generated supercontinuum spectra were characterized at the output of the fiber using a set of fiber-coupled spectrometers, described in more detail below. For pulse compression, spectral dispersion was compensated with either a combination of complementary-paired chirped mirrors (UltraFast Innovations PC1632) and CaF₂ glass or an acousto-optic programmable dispersive filter (AOPDF, Fastlite Dazzler UHR 900 to 1700). Temporal characterization of the few-cycle pulses was performed with a home-built second harmonic generation FROG (SHG FROG) device in single-shot geometry. HHG was performed by focusing the few-cycle pulses into an argon-filled gas cell and the emitted harmonics are dispersed with a concave flat-field grating (Hitachi 001-0640) onto a microchannel plate with phosphor screen detector.

**Spectral characterization**

Because of the poor response of silicon photodetectors for wavelengths above 1 μm, we used multiple spectrometers to capture the full spectral bandwidth. For all measurements in Ar and N₂, the spectra were collected using both a Si-based visible–near infrared spectrometer (Ocean Optics HR 2000 + ES) spanning 180 to 1100 nm and an indium gallium arsenide (InGaAs)–based spectrometer (Ocean Optics Flame-NIR) spanning 940 to 1660 nm. For the broader spectra generated from N₂O, we used an additional cooled InGaAs-based spectrometer (Spectral Evolution IF2500) spanning 1060 to 2600 nm. Using detector response curves provided by the manufacturers, we corrected the collected spectra, interpolated the data to a common wavelength axis, and stitched them in a shared region where both spectrometers are reasonably efficient. Corrected and stitched spectra collected in Ar, N₂, and N₂O for various gas pressures are shown in fig. S1. Individual spectra collected using all three spectrometers for 4.4 bar of N₂O, along with the detector response curves, are shown in fig. S1B to indicate how the spectra were stitched.

**Temporal characterization**

We characterized few-cycle pulses compressed from the generated supercontinuum spectra under three different conditions. The measured and reconstructed FROG traces are shown, along with the retrieved spectra and temporal intensity profiles, in figs. S3 to S5. The specific laser parameters used in each case are also given in their respective figure captions. The FROG trace retrievals were performed using a home-built principal components generalized projections algorithm (37) on a grid of 512 × 512 pixels. FROG retrieval errors are given in the captions of figs. S3 to S5. In N₂ at a pressure of 6.5 bar, we obtain the best dispersion compensation when using eight bounce pairs of chirped mirrors (two reflections each on four pairs of mirrors, providing a group delay dispersion of approximately ~90 fs² per pair) and 20 mm of CaF₂ glass (with a group velocity dispersion of approximately 19 fs²/mm at 1025 nm), resulting in pulses with a full width at half maximum (FWHM) duration of 7.0 fs (two cycles at the central wavelength of 1068 nm). In N₂O at a pressure of 2.4 bar, we compress comparatively lower-energy pulses using five bounce pairs of chirped mirrors (one reflection each on five pairs of mirrors) and 1.5 mm of CaF₂, obtaining pulses with an FWHM duration of 5.8 fs (1.6 cycles at 1074 nm). We also compress a portion of the N₂O spectrum not covered by our chirped mirrors (obtained using the full pulse energy at 3.0 bar) using the AOPDF, after which we obtain pulses with an FWHM duration of 10.4 fs (2.3 cycles at 1374 nm). Because of the low damage threshold of the nonlinear crystal inside the AOPDF, only a small fraction (5 μJ) of the total pulse energy was compressed using the AOPDF.

**High-order harmonic generation**

We generate high-order harmonics by focusing the few-cycle pulses into an argon-filled cylindrical glass cell (inner diameter, 2 mm) and...
characterize them using a flat-field grating spectrometer. The high harmonic spectra from the sub-–two-cycle pulses were generated at a backing pressure of 90 torr, with cell centered approximately 1.7 Rayleigh lengths (3 mm) after the focus. In fig. S6, we compare the spectrum of high harmonic generations from a sub-–two-cycle pulse compressed using N2O-filled HCF to that generated with >3-cycle pulses generated in Xe-filled HCF. As the carrier-envelope phase (CEP) of the laser was not stabilized during these measurements, the harmonic spectra are averaged over all values of CEP. For the sub-–two-cycle pulse, the discrete harmonics merge into a supercontinuum spectrum. The observed harmonic cutoff of 80 eV is consistent with our estimated intensity of 200 TW/cm², based on the experimental focusing conditions, measured pulse energy, and the FROG–retrieved intensity profile.

SUPPLEMENTARY MATERIALS
Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/6/34/eaab5375/DC1

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