One of the challenges of minimally invasive surgery is the dexterous manipulation and precise control of small-diameter continuum surgical instruments. Herein, a magnetic continuum device with variable stiffness (VS) is presented, whose tip is precisely shaped and controlled using an external magnetic field. Based on a low melting point alloy (LMPA), the serial segments composing the continuum device are independently softened via electrical current and remotely deformed under a magnetic torque, whereas the rest of the device is locked in place. The resulting system has the advantage of combining the precision of magnetic navigation with additional degrees of freedom provided by changing the segments stiffness. With a minimum diameter as small as 2.33 mm and an inner working channel, the magnetic continuum device with VS is adapted to use in several therapeutic scenarios, including radio-frequency cardiac ablations and interventional endoscopy in the gastrointestinal tract. The magnetic torque is used to remotely control the shape of the soft sections, whereas the stiff sections remain unchanged, thus adding degrees of freedom to the magnetic continuum device.

1. Introduction

Minimally invasive instruments are inserted in the human body through small incisions or natural lumens, which lead to less trauma and shorter patient recovery time compared to conventional surgical approaches. Among these instruments, flexible continuum devices can safely access difficult-to-reach areas via tortuous pathways, thus enabling new minimally invasive surgical scenarios and enhancing existing therapies. Because the anatomy of body cavities is often complex and patient specific, dexterity and controllability in a confined space are important features for such flexible continuum devices to be successfully used in fields such as neurosurgery and abdominal or cardiac surgery.\textsuperscript{[1]}

To navigate through the workspace, tendon/cable actuation is commonly used for deflecting the tip of continuum devices.\textsuperscript{[2]} For example, in most manual catheters used for radiofrequency (RF) ablation of cardiac arrhythmias, the tip position is controlled by rotating/pushing/pulling the catheter shaft into its sheath and by deflecting the tip with pull wires attached to the distal end of the flexible catheter. Cables, together with other extrinsic actuation mechanisms such as multibackbone structures\textsuperscript{[3]} and concentric tubes,\textsuperscript{[4]} suffer from high friction (e.g., passing tension wires through complex paths) and are limited in their ability to provide multiple bends in a small diameter. Alternative actuation systems include fluidic actuation\textsuperscript{[5]} (usually proposed for larger diameter devices), shape memory alloys\textsuperscript{[6,7]} (raising the issue of precise control), and magnetic actuation.\textsuperscript{[8–10]} In magnetic actuation, an external magnetic field is used to control the pose of the magnetic tip of a continuum device.\textsuperscript{[8]} This remote magnetic navigation approach allows for contactless actuation without the need for transmissions systems running along the device shaft. Unfortunately, even if multiple magnets can be integrated into a single tool, different magnetic field directions cannot be applied at different magnet positions in the workspace inside our magnetic navigation system (MNS). Therefore, it is not currently possible to navigate through the body by adopting multiple curvatures in 2D and 3D without using the support provided by contact with body cavities (e.g., heart walls in the case of cardiac ablation procedures).

Commercially available magnetic catheters are primarily used for treating cardiac arrhythmias,\textsuperscript{[8]} whereas other proposed applications (e.g., brain,\textsuperscript{[11]} lung,\textsuperscript{[12]} cochlear,\textsuperscript{[13]} and eye\textsuperscript{[14]} surgeries) are still far from clinical practice. Such catheters are composed of an ablation tip, flexible segments, and permanent magnets.\textsuperscript{[15]} The number of permanent magnets and the distance between them (i.e., the length of the interposed flexible segment) are optimized for achieving a suitable alignment of the tip to the applied external magnetic field.\textsuperscript{[16]}

To provide stability during operation, the integration of variable stiffness (VS) backbones and outer tubes into nonmagnetically
guided instruments is a well-known solution, particularly for instruments operating in the intestine and abdomen.\textsuperscript{[17]} A number of different designs have been proposed based on tension stiffening of friction-locking beads,\textsuperscript{[18]} combinations of concentric tubes,\textsuperscript{[16]} phase change materials,\textsuperscript{[19]} and granular and layer jamming.\textsuperscript{[20,21]} Among intravascular continuum devices, given the dimension constraints, few examples can be found based on material stiffening (i.e., using materials that undergo stiffness variation under certain stimuli) and are mainly limited to low melting point materials (e.g., polymers\textsuperscript{[22]} and alloys\textsuperscript{[23]}).

In our previous study, we demonstrated the advantages provided by the combination of remote magnetic navigation and VS for minimally invasive continuum devices.\textsuperscript{[24]} Selectively locking one or more flexible segments of a continuum device enables instruments to be capable of several degrees of freedom despite the application of a single magnetic field. Therefore, complex 2D and 3D shapes can be achieved and a wider workspace can be reached. Moreover, the entire structure can be stiffened during a surgical procedure to improve tool stability. The stiffness change is based on a low melting point alloy (LMPA) where serial segments independently undergo a significant stiffness variation (solid to liquid and vice versa) within a biocompatible temperature range (melting temperature below 50 °C).

In this study, we introduce a new design with a central working channel and feedback for closed-loop temperature control (Figure 1). The working channel can be used to connect a functional tip or to insert a tool for applications such as cardiac ablation and gastrointestinal surgery. The closed-loop temperature control averts an overheating and potential damage to the cells. The addition of those two features is achieved without increasing the external diameter of 2.33 mm and overcomes two major limitations of our previous design.

2. Experimental Section

2.1. VS Continuum Devices

We designed and developed different VS continuum devices based on the structure, dimensions, and requirements of existing magnetic catheters.

For efficient shaping, the VS catheter segments should easily bend in the soft state and align in the direction of the magnetic field. For underactuation and stability during end-effector operation, in the stiff state, the VS catheter segments should resist the bending torque due to the magnetic field (i.e., $2 \times 10^{-3}$ Nm) and the contact force between the VS catheter tip and human tissues (e.g., 0.2 N between heart wall and catheter tip during the ablation\textsuperscript{[25]}). The diameter of the VS catheter should be approximately 2.33 mm, which is the current standard for cardiac catheters.\textsuperscript{[26]}

Given the spatial constraints and the mechanical features needed inside the magnetic field, we chose LMPAs as a VS strategy. LMPAs are alloys whose solid/liquid phase change occurs at relatively low temperatures.\textsuperscript{[27]} They are characterized by a large stiffness change upon phase change and by high absolute stiffness when solid.\textsuperscript{[28]} Their potential use in biomedical applications (e.g., micro devices for vessel exploration and material for bone repair) is of current research interest.\textsuperscript{[29]} Among LMPAs, Cerrolow 117 (composition by weight: 45% bismuth, 23% lead, 19% indium, 8% tin, and 5% cadmium) has a 47 °C melting temperature and is stable in air. Below the melting temperature, it is a solid characterized by a Young modulus of 3 GPa, a tensile strength of tens of MPa, and strain at break of around 3% (mechanical characterization described in ref. [28]). Above the melting temperature, the material is a liquid with low viscosity. Cerrolow 117 undergoes phase change faster than other phase change materials (i.e., wax and shape-memory polymer (SMP)) because of its much higher thermal conductivity.\textsuperscript{[30,31]} As the material is liquid at higher temperatures and contains toxic elements such as cadmium and lead, Cerrolow 117 requires encapsulation.

Figure 2 shows the VS continuum device with a central working channel that can be used for active cooling (e.g., irrigation fluid passes through the inner pipe; Figure S1-A, Supporting Information) or cable actuation (e.g., a cable running through the inner channel for actuating a gripper; Figure S1-B, Supporting Information) depending on the surgical scenario. Fabricated according to Figure S2, Supporting Information (see Fabrication in Supporting Information for details), the prototype was composed of an inner flexible tube, Cerrolow 117, three heaters, a magnet, and a silicone tube that encapsulates the entire structure. The external diameter was 2.5 mm. The three heaters consisted of enameled copper wire coiled around the inner tube, corresponding to three independent VS segments (VSSs; see Fabrication in Supporting Information for details). The flexible inner tube was coaxial to the tubular structure.
of the continuum device and was separated by plastic spacers. The spacers were equally spaced on the circumference (120° from each other) and along the length of the flexible tube (15 mm), where they delimited the VSSs (Figure 2, Section B-B). The space between the flexible inner tube and the outer silicone tube was occupied by LMPA. This LMPA distribution allowed for an increased moment of inertia of the continuum device cross-section compared to a backbone-like distribution with the same cross-sectional area, which maximized its bending stiffness in the stiff state. Silicone encapsulation was important not only for containing the molten alloy but also for thermal insulation (thermal conductivity at 100 °C is in the range of 0.2–0.3 W m⁻¹ K⁻¹), electrical insulation, and biocompatibility with human tissues and body fluids.

When current (e.g., 0.8–1 A) was injected into the heaters, the temperature of the LMPA increased above the melting temperature and the VSS becomes soft. In this state, the mechanical performance of the VSS was roughly that of the outer silicone tube. Within an external magnetic field, the soft VSS behaved like the flexible segments in standard continuum devices, allowing the alignment of the magnet with the direction of the magnetic field. When the LMPA solidified inside the magnetic field, the VSS became rigid and retained the deformed shape. In this state, the LMPA core sustained tensile and compressive loads (e.g., due to the magnetic field oriented in a different direction compared to the magnet direction), whereas the contribution to device stiffness from silicone encapsulation was negligible.

A reheating-and-cooling cycle applied to the deformed and/or fractured VSS restored its original straight shape (i.e., the shape of the unloaded silicone encapsulation) and its mechanical properties in the solid state (i.e., Young modulus, maximum stress, and strain). Such a restoration of the mechanical properties after fracture (i.e., self-healing) also occurred in the presence of an external magnetic field.[30] Restoration was due to the prestretched state of the silicone encapsulation obtained during fabrication (see Figure S2 steps D–E and Fabrication, Supporting Information).

The LMPA was radiopaque and, thus, was visible in X-ray images (Movie S3, Supporting Information). During an ablative procedure, this feature allowed the electrophysiologist to monitor the position of the catheter with a mapping system and a fluoroscope.

Each heater, which was implemented by enameled copper wire wrapped around either the flexible inner tube or directly on the LMPA, was a closed electric circuit. One end of the copper wire runs along the encapsulated structure to the base (i.e., toward the external part of the device; see Fabrication in Supporting Information). One part of the copper wire constituted the heater itself, being tightly wrapped around the section to be heated. The second end of the copper wire was connected to ground either externally (i.e., by running along the structure to the base like the other end) or through the LMPA (see Fabrication in Supporting Information).

### 2.2. Stiffness Control

As previously mentioned, the stiffness of each VSS depends on the phase of the LMPA, which can be locally and independently changed by Joule heating. The enameled copper wires wrapped around the core of the catheter (see Section 2.1 and Fabrication, Supporting Information) define separate VSSs and serve as both heaters (where current is injected to melt the LMPA) and temperature sensors. This minimizes the number of electric wires running along the structure, decreases device complexity, and increases space for other components. The temperature of the heater $T_h$ is related to the copper wire resistance $R_h$ as

$$R_h = R_0(1 + \alpha(T_h - T_0))$$

(1)

where the temperature coefficient $\alpha$ of the copper is equal to $3.9 \times 10^{-3} \cdot ^\circ \text{C}^{-1}$, and $R_0$ is the wire resistance at an initial temperature $T_0$.

In a surgical scenario, the temperature varies between 37 °C (body temperature) and 47 °C (melting temperature of the LMPA). This implies that very low resistance variations must be monitored. Resistance measurement was performed with a high precision resistance measurement terminal (EL3692, Beckhoff Automation AG, Germany) connected to the heater with a four-wire connection in parallel with a power supply. The components of the setup were coupled to an EtherCAT fieldbus, and the overall setup was controlled with a TwinCAT PLC Control running a real-time operating system. Heating was performed by applying a pulse-width modulation (PWM) voltage signal across the heater. The resistance measurement was performed on each low state of the PWM signal so that both heating and resistance measurements were performed alternatively using the same wires. The current used for the resistance measurement was lower than 45 mA, and its influence on the wire heating was negligible with respect to the heating current produced by the power supply (i.e., 0.8–1 A).

A VSS was maintained in the soft state by injecting current so that the heater resistance remains between the lower and upper
bounds using a hysteresis controller. The lower bound was set slightly above the resistance corresponding to the LMPA melting temperature. The upper bound was set close to the lower bound to avoid overheating the LMPA. Both resistance thresholds were experimentally identified with initial testing of the device (see Section 3.1).

2.3. Actuation and Modeling

2.3.1. Magnetic Actuation

Remote magnetic navigation was performed with an MNS. Such systems usually use either static electromagnets or moving permanent magnets to generate a magnetic field within a given volume.\[32\] The permanent magnet embedded at the distal end of the flexible continuum device was subjected to a magnetic torque that attempts to align it with the external field direction, allowing control of the device tip position with the MNS. In an external magnetic field $B$, the magnet in the continuum device tip, characterized by a magnetic dipole $m$ and a position $p$, experiences a magnetic torque

$$T_m(m, p) = m \times B(p)$$

(2)

This torque is proportional to the magnetic field magnitude. It is equal to zero when the magnetic dipole $m$ is aligned with the magnetic field $B$ and is maximal when $B$ and $m$ are orthogonal if the magnetic material on the catheter is permanently magnetized.\[33\]

2.3.2. Device Modeling

The magnetic continuum device is modeled with an Euler-Bernoulli beam model assuming a constant curvature along the length of the device, as previously proposed in ref. [34]. Using the same assumption as Tunay for a thin body,\[35\] we assume that the plane sections of the continuum device remain in-plane and perpendicular to the neutral-fiber axis after deformation, and the shear deformation is negligible. In this case, we have

$$\kappa = \frac{T_m}{EI}$$

(3)

where $T_m$ is the bending moment, $E$ is the Young modulus of the elastic material, $I$ is the area moment of inertia, and $\kappa$ is the segment constant curvature.

Equation (2) is rewritten using the magnetic field norm $B$ and the dipole moment norm $m$ to obtain the magnetic torque norm:

$$T_m = B_m \sin(\gamma - \theta)$$

(4)

where $\gamma$ denotes the magnetic field inclination angle and $\theta$ is the inclination angle of the tip magnet. From Equation (4), we can observe that a misalignment angle $\gamma - \theta$ between the external magnetic field and migration direction is required to apply a control torque on the magnet. No magnetic torque can be generated around the dipole axis. For the considered device and magnetic field intensity, the influence of gravity on the device position is negligible. The influence of the force produced by the magnetic gradients is also negligible, as the magnetic field produced by the MNS is essentially homogeneous.

Using the conversion between magnet inclination angle and curvature $\theta = \kappa l$ and, combining Equation (3) and (4), we obtain

$$\theta = \frac{1}{EI} \sin(\gamma - \theta)$$

(5)

The relation between $\theta$ and $\gamma$ can be obtained by searching the root of the function for a give $\gamma$. To avoid an unstable state when $\gamma$ reaches 180° (i.e., no out-of-plane torque to maintain the catheter in the azimuthal plane), $\gamma$ must remain less than 180°. The flexural rigidity can be estimated using the relation introduced in Equation (5).

2.3.3. Forward Kinematics of the Magnetic Continuum Device

The majority of continuum devices use insertion/retraction and shaft rotation to control distal tip position. In cardiac surgery, the RF catheter is inserted into the heart chamber through a semirigid insertion sheath, which allows for the transmission of the insertion and rotation motion along the catheter shaft. Endoscopes for navigation in the gastrointestinal tract have a 2.8 mm tool channel, and insertion or rotation motion can be transferred to the distal end as for cardiac catheters. Mechanical rotation motion is represented by $\phi_0$ and the mechanical translation motion by $d_0$. The resulting transformation for the mechanical motion is

$$T_0^1 = \begin{pmatrix}
\cos(\phi_0) & -\sin(\phi_0) & 0 & 0 \\
\sin(\phi_0) & \cos(\phi_0) & 0 & 0 \\
0 & 0 & 1 & d_0 \\
0 & 0 & 0 & 1
\end{pmatrix}$$

(6)

Assuming a constant curvature, a continuum device can be defined by a set of arc parameters.\[36\] The constant curvature arc is defined by a curvature $\kappa$, an in-plane rotation angle $\phi$, and a segment length $l$. The coordinate system for the distal end is set at the distal end of the insertion sheath or the tool channel with the z-axis aligned with the continuum device longitudinal axis. The configuration space is parameterized with $q = [\phi_0, d_0, \phi_1, \kappa_1, l_1, \phi_2, \kappa_2, l_2, \phi_3, \kappa_3, l_3]$ for a two-segment VS continuum device, with the index representing the ith segment.\[37\] The resulting transformation for one VSS is

$$T_i^1 = \text{rotz}(\phi_1)T_{\text{inPlane}}(\kappa_1l_1) = \begin{pmatrix}
\cos(\phi_1) \cos(\kappa_1l_1) & -\sin(\phi_1) \\
-\sin(\phi_1) \cos(\kappa_1l_1) & \cos(\phi_1) \\
-\sin(\kappa_1l_1) & 0 \\
0 & \cos(\kappa_1l_1)
\end{pmatrix}$$

(7)
When the curvature is zero the transformation is given by
\[
T^1 = \text{rot}_z(\phi_1) T_{\text{inPlane}}(\kappa_1; l_1) = \begin{pmatrix}
\cos(\phi_1) & -\sin(\phi_1) & 0 & 0 \\
-\sin(\phi_1) & \cos(\phi_1) & 0 & 0 \\
0 & 0 & 1 & l_1 \\
0 & 0 & 0 & 1
\end{pmatrix}
\] (8)

To combine the motion from multiple VSSs, the transformation matrices for each segment are multiplied.

3. Results

3.1. Thermal Characterization

Thermal characterization of the VS continuum device is performed in air at room temperature (24 °C) and in water at body temperature (37 °C without forced flow) to mimic a real-case scenario. The surface temperatures of the device are measured by two thermistors (SMD 0402, Vishay) glued on the device’s external surface at the center of one of the heaters (measuring temperature $T_1$) and 10 mm away from the heater center (measuring temperature $T_2$). The device is heated for the first 60 s of the experiment. For the rest of the experiment, no current is applied and the heater naturally cools in the environment. The heater has a resistance $R_0$ of 2.15 Ω at $T_0 = 24$ °C with the wires extending 100 mm outside of the heater. The wires are connected to a larger cross-section wire to limit the self-heating of long connecting wires. The maximum current in the heater is limited to 1 A to avoid damage to the heating wire. The resulting variations of the resistance of the heater are shown in Figure 3A and corresponding temperature measures in Figure 3B.

In both air and water, the melting and the solidification of the LMPA are indicated by the two plateaus clearly visible on the heater resistance measurement during the heating phase (at $R = 2.30 \Omega$) and the cooling phase (at $R = 2.27 \Omega$). This shows that stiffness control can be robustly performed using the resistance measurement. Thresholds for the hysteresis controller can thus be selected based on this experiment, after identification of the plateau corresponding to the phase change of the LMPA. One can see that the thermistors’ temperatures on the corresponding plateau are different in air and water. This can be explained by the fact that the thermistors are mounted on the outer surface of the silicone tube and are not directly in contact with the heater.

The maximum temperatures reached after the heating process in air and water are 60 °C and 41 °C, respectively, on the outer surface of the device.

The melting time (i.e., the time needed to completely melt the VSS during the heating phase) is ≈15 s in both cases. Starting from a temperature of 41 °C, which constitutes the higher thermal limit to avoid damage to the body, the cooling time needed for the complete solidification of the VSS is faster in water (20 s) compared with air (80 s), consistent with the relative high heat transfer capability of water with respect to air.

The stiffness transition (solid to liquid) can be obtained in water with external temperatures $T_1$ and $T_2$ less than 41 °C, thus ensuring no thermal damage to human cells.

3.2. Stiffness Control Demonstration

To test stiffness control, a VS continuum device is placed inside a rotating magnetic field and is maintained in the soft state with a hysteresis controller. The magnetic field oscillates between $-90^\circ$ and $90^\circ$ with an angular speed of $30^\circ \text{s}^{-1}$; at $90^\circ$ and $-90^\circ$, the magnetic field is maintained constant for 1 s. The rotating magnetic field is used to measure the deflection amplitude over time. The heating starts at $t = 0$ s when the active hysteresis controller turns on the heating, and Figure 4A shows the heater resistance and deflection amplitude over time. During the first 20 s, we observe the plateau corresponding to the LMPA phase change between solid and liquid, and after turning off the heater, the plateau corresponding to the LMPA phase change from liquid to solid.

In Figure 4B, the correlation between deflection amplitude and heater resistance is shown. The deflection amplitude is measured between two deflection peaks and is an average between two discrete measurements separated by 7 s. The point $t1$ on

![Figure 3](image-url) **Figure 3.** Results of thermal characterization in air at 24 °C (red) and in water at 37 °C (blue). A) Representative curves of the heater resistance over time in the two cases. B) Representative curves of the surface temperature measured with thermistors corresponding to the heater ($T_1$) and 10 mm from the heater ($T_2$).
the plot represents the resistance at \( t = 12 \) s and the deflection amplitude between measurements at 5 and 12 s. The initial heating is too fast to provide a reliable measurement of deflection amplitude variation because the deflection was close to zero at 5 s and close to the steady state at 12 s. Once the LMPA is melted, the hysteresis controller maintains the resistance between the thresholds to avoid overheating or LMPA solidification. This results in maintaining the deflection amplitude close to a constant value of 30°.

In the soft state, the magnetic field inclination was varied between 0° and 150° in both directions. As shown in Figure 5B–D, it is possible to deflect each of the VSS segments independently more than 100°. The deflection of VSS1 was larger because it carries the weight of the two distal segments and the tip magnet. Using Equation (5) and an estimation of each parameter, we obtain an estimate for the flexural rigidity of \( 5 \times 10^{-6} \) Nm².

To increase the deflection of a single VSS, the magnetic volume or the magnetic field can be increased. Depending on the desired operating volume, the VSS length can also be increased. In this case, a length increase has the advantage of not being affected by a possible nonlinearity of the elasticity module for large deflection angles.

The current injected into the VSS generates a magnetic torque that is negligible, being approximately two orders of magnitude smaller than the one generated by the permanent magnet. No impact of the additional dipole moment because of the heaters has been observed when turning on and off the heater in a static magnetic field while one of the segments is in a soft state.

### 3.3. Deflection in Soft and Stiff States

Two key device characteristics that must be determined are softness and stiffness. Softness is determined by deflection in a specific magnetic field when one of its segments is in the liquid state. Stiffness is determined by investigating the effect of the magnetic torque when the segments are in their solid state, which governs the level of shape fixity that can be achieved. The deflection for our VS continuum devices prototype is characterized inside the CardioMag (the Aeon Phocus nonclinical prototype) with a magnetic field magnitude of 80 mT and varying magnetic field orientations. The VS continuum device tested has three segments. A hysteresis controller was used to maintain a VSS in the soft state.

In the rigid state, the VSS is not significantly deflected at the maximum magnetic torque of \( 2 \times 10^{-1} \) Nm, which is obtained by applying a magnetic field magnitude of 80 mT and a misalignment angle of 90° (Figure 5A). The configuration of the overall catheter does not influence its shape fixity capability within this range of torques and tip curvatures.

In the soft state, the magnetic field inclination was varied between 0° and 150° in both directions. As shown in Figure 5B–D, it is possible to deflect each of the VSS segments independently more than 100°. The deflection of VSS1 was larger because it carries the weight of the two distal segments and the tip magnet. Using Equation (5) and an estimation of each parameter, we obtain an estimate for the flexural rigidity of \( 5 \times 10^{-6} \) Nm².

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The current injected into the VSS generates a magnetic torque that is negligible, being approximately two orders of magnitude smaller than the one generated by the permanent magnet. No impact of the additional dipole moment because of the heaters has been observed when turning on and off the heater in a static magnetic field while one of the segments is in a soft state.

### 3.4. Constant Stiffness Workspace

A constant stiffness workspace is a workspace that can be explored without a change of stiffness, which means that there are no heating or cooling delays (Figure 6A and Movie S4, Supporting Information). During an minimally invasive surgery (MIS) procedure, it would be of particular interest to operate in one of these constant stiffness workspaces.

From the measured deflection characteristics of our VS continuum devices, we can simulate the reachable workspace assuming constant curvature using the forward kinematics (Section 2.3.3). To select a constant stiffness workspace and the corresponding continuum device shape, we can explore all

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Figure 4. Results of stiffness control for a variable stiffness catheter. A) Measurement of heater resistance and deflection amplitude in a rotating magnetic field between –90° and 90° in air. B) Correlation between resistance and tip deflection amplitude.
continuum device shapes for reaching target positions. A simplification for exploring all possible shapes can be obtained by observing that the parameters $\phi_0$ and $\phi_1$ define a rotation around the same axis. Removing the mechanical rotation does not reduce the possible continuum device shapes and final position but does reduce the number of trajectories to reach these end effector positions. To determine all possible configurations to reach a target position in task space we can compute all possible continuum device shapes for varying parameters, excluding $\phi_0$, $\phi_1$, and $d_0$. The set of configurations that have the same radial distance from the insertion axis can reach the position in task space by mechanical insertion $d_0$ and mechanical rotation $\phi_0$. In Figure 6B, the planar continuum device configurations that reach a target position are represented. It can be observed that a variety of continuum device shapes with different tip orientations can reach a single target position. This can be extended to nonplanar shapes to further increase the diversity of configurations and tip orientations.

Figure 5. Cumulative image representing the deflection of our VS magnetic continuum devices. A) The three VSSs are in rigid states and magnetic field inclination is changed between $-90^\circ$ and $90^\circ$. B) VSS1 in the soft state and magnetic field inclination is changed between $150^\circ$ and $150^\circ$. C) VSS2 in the soft state and magnetic field inclination is changed between $-150^\circ$ and $150^\circ$. D) VSS3 in soft state and magnetic field inclination is changed between $-150^\circ$ and $150^\circ$.

Figure 6. A) Composition of sets of catheter configurations in a constant stiffness workspace (VSS1-2: rigid, VSS3: soft). B) Set of planar configurations to reach a target tip position.
Each of the continuum device configurations results in a different constant stiffness workspace. A well-selected constant stiffness workspace reduces the number of stiffness changes required during a particular procedure and thus reduces the time it takes to perform a given task.

### 3.5. Mechanical Actuation and Magnetic Actuation

In a given stiffness state, the degrees of freedom available are the mechanical rotation, mechanical insertion/retraction, and tip deflection with the magnetic field. With the VS continuum device inserted inside an introducer sheath, the mechanical insertion/retraction moves the continuum device tip in a motion collinear to the insertion axis (Figure 7A) and the mechanical rotation in a circular trajectory centered on the insertion axis (Figure 7B). Creating a contact between an MIS instrument and organ tissue requires the ability to move the tip of an instrument forward. This motion is primarily performed by mechanical insertion and rotation. Tip deflection changes the instrument orientation but not its length. In a constant stiffness state, simultaneous control of the tip position and orientation (i.e., six degree of freedom (DOF)) is not possible, because there are only four control variables, but for purely position control, we have one redundant control parameter. This means that hysteresis and error in the rigid segments shape can be corrected with mechanical actuation and magnetic actuation.

The position precision depends on the precision of the position feedback system and the closed-loop control algorithms. The mechanical actuation and magnetic actuation allow precise and fast motion with delay less than 200 ms allowing an algorithm to close the loop and achieve submillimeter position precision.\(^{38}\) Hysteresis and error in the mechanical actuation and magnetic actuation can be directly compensated by closed-loop control.

In a scenario close to a cardiac arrhythmia ablation, we demonstrated that the user can control the magnetic field direction at the center of the workspace and the catheter insertion length to reach a target tip position.\(^{10}\) The uniformity of the magnetic field in the workspace is sufficient, and inhomogeneity of the magnetic field does not disturb the user. Similar results are expected with our VS continuum device, because in a given stiffness state the dynamics are similar to a conventional magnetic catheter, and fine position control only relies on mechanical actuation and magnetic actuation.

The VS has been shaped repeatedly with the magnetic field for more than 5 h without observable fatigue (Movie S6 in Supporting Information shows 600 s of operation). In our previous prototype without an inner lumen,\(^{24}\) fatigue was observed because of rigid deformation of the copper wire. The inner lumen not only provides a working channel, but also maintains the heating wire in its original position.

### 4. Discussion and Conclusion

The VS magnetic continuum device provides a significant increase in manipulability compared to available magnetic continuum devices. Its small diameter and central working channel allow its use in several minimally invasive procedures in organs with small diameter access paths such as heart chambers and the gastrointestinal tract. If the VS magnetic continuum device is used in the context of cardiac arrhythmia ablation, it enables multiple bending radii and reduces the number of magnets from 3 to 1 compared with traditional magnetic catheters. It can be selectively softened for deflection under the magnetic field or can be rigidified for better stability. Due to the multiple VS sections and integrated temperature control, the deformation can be locally controlled in tens of seconds, enabling, for example, a part of the VS catheter to maintain an optimal compliance for a larger range of

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**Figure 7.** A) Representation of the insertion constant stiffness workspace in cyan with the set of continuum device distal positions (blue circle) for a given insertion length. B) Representation of the rotation workspace in cyan with the set of continuum device tip distal positions (blue circle) for a given rotation angle.
insertion lengths. For gastrointestinal endoscopy, the VS magnetic continuum devices can be directly inserted into the tool channel (internal diameter ranging between 2.8 and 3.8 mm depending on the particular endoscope\(^{[10]}\)) of existing endoscopes to provide precise tool control and multiple bending locations without increasing the overall endoscope diameter.\(^{[10]}\)

With the increased dexterity comes new challenges that will require the development and integration of 3D shape detection algorithms, path planning algorithms, closed-loop control algorithms, a mechanical advancer unit, and an intuitive control interface for the surgeon. In addition, fundamental work on thermal modeling, thermal control, characterization methods, and improvement of the manufacturing process is needed.

**Supporting Information**

Supporting Information is available from the Wiley Online Library or from the author.

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**Conflict of Interest**

The authors declare no conflict of interest.

**Keywords**

continuum robots, magnetic navigation, medical robotics, soft robotics, variable stiffness system

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