Electronic Properties and Scanning Tunneling Microscopy Simulation of MoS₂ Nanosheets by Using Density Functional Theory

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Abstract

The ab-initio Density Functional Theory (DFT) approach is used to study the electronic properties of bulk and layered MoS₂ nanosheets. For the layered structures mono, bi, tri, tetra and penta layered structure is used. The direct to indirect transition of bandgap is observed as the number of layers is increasing. This transition of bandgap is attributed to the van der Waals interlayer interaction between two layers of MoS₂ nanosheets. The indirect bandgap in the bulk MoS₂ is found to be 0.94 eV, whereas for a single layered nanosheet is found to be direct bandgap with the value of 1.83 eV. To confirm the surface termination and understand the surface morphology of MoS₂ the scanning tunneling microscopy (STM) simulation is performed in constant height mode. It is found that the detection of surface atoms via STM depends on the tip atom of the STM.

Keywords: Bandgap, van der Waal’s, catalysis, STM tip, indirect bandgap

I. Introduction

Layered transition-metal dichalcogenide (TMDC) nanosheets have attracted attention due to their potential application in nano electronic devices, spintronics, optoelectronic devices, catalyst, effective solid lubricant, and electrochemical sensors. Amongst the TMDCs, molybdenum disulfide (MoS₂) is very cheap and easily available. In a bulk MoS₂ hundreds of single layers are stack together with van der Waal’s force. Since van der Waal force is very weak, to separate a single layer from a bulk sample of MoS₂ is very easy. Each layer of MoS₂ has a plane of hexagonally arranged Mo atoms sandwiched between two planes of hexagonally arranged S atoms, with the covalently bonded S-Mo-S atoms in a trigonal arrangement forming a hexagonal crystal structure. The theoretical formation of a single layer MoS₂ from its bulk structure is rather easy which can be created by deleting some of the adjacent layers.

Electronic properties change drastically when MoS₂ is reduced from bulk to a single layer. The MoS₂ monolayer has unique mechanical, electrical, optical and chemical properties. This uniqueness of single layered MoS₂ make it very useful in practical applications, and the morphology of a layer is very important for practical device fabrications. It has been suggested that the electronic properties of MoS₂ have a strong dependence on the number and distance of planes composing the system. Based on this transition from direct to indirect bandgap, a single layer MoS₂ was used to construct a transistor. The direct bandgap monolayer also demonstrates strong photoluminescence as a result of quantum confinement.

It was found in the scanning tunneling microscopy (STM) experiment by Tianshu Li and Giulia Galli that the morphology and electronic properties of MoS₂ nano flakes depends on the size of the flacks. The size and the morphology of the nanoparticles was found to have strong dependence on the nature of surface atoms of the nanoparticles. The nanoparticles with large number of S atoms on the surface has much profoundness than the Mo atoms on the surface of the nanoparticles, which indicate that the S covered nanoparticles are energetically more favorable than the Mo covered one.

To understand the electronic and morphological properties of MoS₂ nanolayers, we have carried out systematic electronic structure calculations. The ab initio density functional theory (DFT) is used for the simulation of electronic structures. The most widely used method for theoretical calculations is DFT since it considers the quantum mechanical interaction of the electron and ions of the materials into account. In DFT formalism the electronic density of the materials is considered to be the source of all physical and chemical properties of a material rather the position and number of electrons. A detailed theoretical study of single-layer and multi-layer structures MoS₂ nanosheet is also performed in this work. The scanning tunneling microscope (STM) images can be obtained from the density of states (DOS) of the surface atoms of the semiconducting materials. We have used the Tersoff-Hammen approximation to study the surface morphology of the MoS₂ surface.

II. Computational Details

The DFT approximation as implemented in the Viena Ab-initio Simulation Package (VASP) is used to carry out all the calculations. The electronic exchange and correlation effects are included by Perdew-Burke-Ernzerhof (PBE) pseudo potential which uses the generalized gradient approximation (GGA). The Projected Augmented Wave (PAW) technique was used to describe ion-electron interactions. The effect of van der Waals interactions is included by using the D3 correction scheme of Grimme with Becke-Jonson damping. The cut off energy for the plane wave basis was set as 600 eV. The Gamma centered k-sampling is used as KPOINTS and the 12x12x12 k-points are used for the bulk calculations. For the layered MoS₂ we have used 12x12x1 k-points mesh since the layers are infinite in x and y directions and finite in z direction. For the nanoparticles only a single k-point centered at gamma point in the Brillouin zone is used. Visualization for Electronic and Structural Analysis (VESTA) software was

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used to model the initial structures. For modeling of the layered structures, a gap of 6 Å is included along the z-direction both on the upper and lower side of the layer, so that a layer cannot have Coulombic interaction between its periodic images. Conjugate gradient algorithm is used for ionic relaxation and the ions are allowed to move freely in all three directions in space. The force convergence criterion was set to 0.01 eV/Å.

**III. Results and Discussion**

*Bulk and Layered MoS$_2$ nanosheets*

MoS$_2$ is a layered 2D material and there is van der Waals interaction exist between two adjacent layers. The unit cell of MoS$_2$ consist of two layers of S-Mo-S. The optimized bulk structure of MoS$_2$ is shown in the Fig 1(a), it has structural symmetry of P6$_3$/mmc with a layer staking 2Hc type. The hexagonal lattice constant is obtained to be 3.20 Å, the height of a single S-Mo-S layer is 3.16 Å, and the separation between two adjacent S-Mo-S layers is found to be 3.00 Å. These values are in good agreement with the experimental values obtained by T. Boker et al$^{17}$ and with other DFT calculation$^{18}$.

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**Fig. 1.** (a) Bulk, (b) Monolayer, (c) Bi layer, (d) Tri layer, (e) Tetra layer, and (f) Penta layer of MoS$_2$ nanosheet. Mo atoms are indicated by purple(black) balls and S atoms are indicated by yellow (white) balls.

**Fig. 2.** Left panel represents the DOS and right panel represents the band structures of (a) mono-layer, (b) bi-layer, (c) tri-layer, (d) tetra-layer, and (e) penta-layered MoS$_2$ nanosheet, respectively.
The monolayer, bi-layer, tri-layer, tetra-layer, and penta-layer MoS2 slabs were made from the optimized bulk structures and it is again relaxed with the DFT approximation. The optimized structures are shown in the Fig 1(b-f).

After geometry optimization and static calculation, we have studied the band structure of the MoS2 and plot the band structure along the Γ–M–K–Γ path using the relaxed lattice parameters, as represented in the right side of the Fig 2. The van der Waals interaction were present for all the structures expect for the monolayered one. Our calculated value of the indirect bandgap is found to be 0.94 eV for bulk MoS2, which is in agreement with the experimental bandgap. For the monolayered nanosheet the direct bandgap of 1.83 eV is found. The reported value of experimental bandgap for the mono-layer structure is ~1.90 eV. For bilayer, tri layer, tetra layers and penta layered structures, the bandgap is indirect and the value is 1.24 eV, 1.05 eV, 0.68 eV and 0.00 eV, respectively. The experimental indirect band gap for double layer MoS2 structure is ~1.26 eV and tri-layer is ~1.20 eV according to earlier published works. Our calculated values of bandgap are in close agreement with available experimental results. The density of states (DOS) for all these structures are shown in the left panel of Fig 2. It is shown that DOS is symmetric for both spin up and spin down atoms. This indicates that MoS2 nanosheets are non-magnetic. The bandgap is decreasing with the increasing of number of layers in the structures. For the case of five layered and more the semiconducting MoS2 showed metallic behavior, which is not consistent with other calculations and experimental findings. This disagreement is due to the van der Waals force we incorporated among the layers in our theoretical calculations. This may be due to the effectiveness of the large van der Waals force between the layers. It is clear from the Fig 2 that with the increasing the number of layers the valance band maxima is shifting from the K points towards the Γ point, and the conduction band minima is moving to the opposite direction. This shifting of conduction and valance band edge may have significant effect on the optical absorption of the MoS2 nanosheet.

As the number of layers of MoS2 increases, the band gap monotonically decreases. MoS2 nanosheets have radically different properties compared to the bulk system. For finite number of layers, the interlayer van der Waals interactions is being removed, the itinerant electrons get confined due to the finite size effect of the nanosheet which leads to the direct bandgap as contrary to the bulk MoS2. The indirect to direct transition of the bandgap is shown in the Fig 3, which is consistent with the previous calculations. Direct band gap in two-dimensional transition metal dichalcogenides depends on the localized d orbital of transition metal, and due to the location in the unit cell, these are slightly affected by the interlayer coupling. But the indirect bandgap depends on the overlap of d orbital of transition metal and p orbital of chalcogenide atoms which depends on the interlayer coupling. Bulk and multi-layered structures are found to have indirect bandgap whereas monolayer structure has a direct bandgap.

![Fig. 3. Transition from indirect to direct bandgap of (a) bulk and (b) monolayer of MoS2](image)

As we moved from the monolayer to bi-layer, tri-layers, and tetra-layers MoS2 nanosheets, the direct bandgap again converted to indirect bandgap like the bulk MoS2. This is due to the reason of van der Waals interaction between the layers, which was absent for the mono layer MoS2 nanosheet. The quantum confinement of electrons in the monolayer MoS2 make this nanosheet suitable for catalytic applications, and the bandgap of layered MoS2 is suitable for photovoltaic applications. The band gap of the bulk and up to five layers of MoS2 nanosheets are summarized in Table 1.

| Number of layers | CBM (eV) | VBM (eV) | Band Gap (eV) | Nature of Band Gap |
|------------------|---------|---------|--------------|-------------------|
| 1                | 1.58    | -0.25   | 1.83         | Direct            |
| 2                | 1.03    | -0.21   | 1.24         | Indirect          |
| 3                | 0.82    | -0.23   | 1.05         | Indirect          |
| 4                | 0.45    | -0.24   | 0.68         | Indirect          |
| 5                | 0.40    | -0.04   | 0.45         | Indirect          |
| Bulk             | 0.72    | -0.22   | 0.94         | Indirect          |

**STM Simulation of MoS2 Surface**

It is a long-standing debate whether the MoS2 surface is terminated by S atoms or by Mo atom because the identical structure of S and Mo surface lattice. To observe the surface termination and morphology of clean MoS2 1X1 surface, we have applied the Tersoff-Hamman approximation to simulate the STM images. The tunneling current I is measured as a function of tip position by the equation 1.

$$I = \sum_{\psi_s} |\psi_s|^2 \delta(E_s - E_F) = \rho(r, E_F)$$  \hspace{1cm} (1)$$

Where $E_s$ is the energy of the s’th Khon-Sham orbital, $E_F$ is the energy of the Fermi level and $\psi_s$ is the wavefunction of the s’th Khon-Sham orbital. The electron density is given by $\rho(r, E_F)$ near the Fermi energy. The electronic density is calculated around the Fermi energy by using the VASP code and plot them in a constant height of the iso-surface to produce the STM image.
In the MoS$_2$ unit cell the $d_{z^2}$ orbital of Mo is situated on top of the valance band which may be responsible for the appearance of Mo atoms on the STM images, on the other hand the attenuation of d orbital as compared to the s or p orbital can play role to visualize S atoms rather than Mo atoms in the STM image. We have used Tersoff-Hamman approximation there is no direct electronic mixing between the tip atom and surface atom within this approximation. To do this with the VASP package, we first complete a self-consistence force (scf) calculation of a 1x1 MoS$_2$ surface, and then we generate the partial charge of the system, once the partial charge is generated, the iso-surface of the charge is plot via the VESTA code, which is basically the STM image of the system. Clean MoS$_2$ (1x1) surface was scanned using negative bias voltage of -1 V and positive bias voltage of +1 V using three different tips (Tungsten tip, Molybdenum tip) in the constant height mode. Tip apex atom was kept at a fixed height of 4 Å from the top surface atom in all scans. Resulting tunneling current from (to) sample (tip) was recorded.

Fig 4(a) shows the resulting STM image of MoS$_2$ (1x1) cell using tungsten tip, the left image is for -ve bias potential and the right image in Fig 4(a) is for positive bias potential. In both cases of negative or positive bias potential. In the case of molybdenum tip with -ve bias Fig 4(b) and sulfur tip with both positive and negative bias Fig 4(c) Sulphur atom are being seen in the STM image. In the case of molybdenum tip with +ve bias, molybdenum atom is being imaged.

To understand the STM image presented in Fig 4, we have calculated the projected density of states (PDOS) of both the tip atoms and the surface atoms of MoS$_2$ as presented in the Fig 5(a) and Fig 5(b) respectively. The total DOS for all the three tips have very large DOS near the Fermi level as seen in Fig 5(a). For the W tip the $d_{xz}$ orbital large density near the Fermi level in the unoccupied states. This is the conduction band minima of the W atom, this $d_{xz}$ orbital will contribute to the image formation when scanned the MoS$_2$ surface, and the greater contributing orbital for the case of Mo tip is also $d_{xz}$. The $d_{z^2}$ orbital has a peak at an energy around 1.0 eV in the unoccupied side and around -1 eV energy in the occupied side. This orbital may contribute to the STM images for the case of 1.0 eV potential in either positive or negative bias. For the case

![STM images of 1x1 MoS$_2$ with (a) Tungsten tip. Left is with -ve bias potential, and right is with +ve bias potential, (b) Molybdenum tip. Left is with -ve bias potential, and right is with +ve bias potential.](image)

**Table 2.** Type of atom imaged with respect to type of tip atoms and nature of applied bias potential

| Tip Atom      | Negative bias | Positive bias |
|---------------|---------------|---------------|
| Tungsten (W)  | S             | S             |
| Molybdenum (Mo)| S             | Mo            |

**IV. Conclusions**

The structural and electronic properties of MoS$_2$ nanosheets of various sizes, shapes, and geometries have been studied. The electronic structure studies of monolayer, bilayer, trilayer, tetralayer and pentalayer have been performed. The bandgap of the bulk MoS$_2$ is found to be 0.94 eV, which is consistent with other studies. The bandgap of the layered nanosheets are increasing as the number of layers are increasing. The maximum obtained gap is 1.80 eV for the monolayer MoS$_2$ nanosheet. There is indirect to direct transition of band gap from bulk to monolayer of MoS$_2$. The simulated STM images showed that sulfur atoms have larger electronic density near Fermi level since they are clearly imaged under STM. The symmetric DOS and PDOS
of these structures indicate the non-magnetic nature of these MoS$_2$.

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