Predictive values, uncertainty, and interpretation of serology tests for the novel coronavirus

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Antibodies testing in the coronavirus era is frequently promoted, but the underlying statistics behind their validation has come under more scrutiny in recent weeks. We provide calculations, interpretations, and plots of positive and negative predictive values under a variety of scenarios. Prevalence, sensitivity, and specificity are estimated within ranges of values from researchers and antibodies manufacturers. Illustrative examples are highlighted, and interactive plots are provided in the Supplementary Information. Implications are discussed for society overall and across diverse locations with different levels of disease burden. Specifically, the proportion of positive serology tests that are false can differ drastically from up to 3%–88% for people from different places with different proportions of infected people in the populations while the false negative rate is typically under 10%.

The SARS-CoV-2 pandemic is wreaking havoc on physical, mental, economic, and general societal health. Potential treatments for Covid19 currently have limited evidence of efficacy. Thus, it is critical to develop agents to prevent the spread of coronavirus, such as vaccines. Although research and development on vaccine candidates is ongoing, widespread availability of a safe and effective vaccine is not expected for months or even years. Simultaneously, there is increasing evidence of asymptomatic infection and spread. With scarce testing supplies, many people, blind to their prior infection status or lack thereof, are self-isolating; the current situation has even consequently been derided as Schroedinger’s virus.

Without a vaccine, excitement about antibodies testing is growing. Theoretical benefits of identifying individuals with antibodies abound. Daily activities such as shopping, traveling, and dining could begin to resume, alleviating currently acute social and economic effects of the pandemic. Hoping to implement these potential benefits, some politicians have considered issuing immunity passports for people who are cleared by an antibodies test. Yet, serology testing is not a panacea, and is associated with concerns about its use.

Given the increase in testing, proper interpretation of the results is critical with implications for medicine, public policy, and personal action. The goal of this paper is to estimate, quantify and visualize uncertainty in the predictive values and false positive rates of serology testing candidates available at the time of writing. Graphical displays of predictive values feature a range of scenarios. "Background" reviews key metrics for serology tests. "Results" summarizes and visualizes metrics in general and for serology tests operating under an Emergency Use Authorization (EUA). "Application to specific locations" applies the concepts to specific locations in the United States (US). "Discussion" discusses limitations and implications. Finally, "Methods" details our statistical and graphical methods.

Background
This section outlines key statistical definitions related to serology testing. Readers familiar with testing characteristics may skip to "Results". Definitions are included in the Supplementary Information. Additional details on these concepts and examples relevant to serology may be found elsewhere.

Two properties of serology tests quantify how well the tests perform in on samples in a lab with known antibody status. Sensitivity is the probability that a serology test correctly classifies a sample with antibodies for SARS-CoV-2. According to the FDA, sensitivity of a test refers to its “ability to identify those with antibodies to SARS-CoV-2” and “can be estimated by determining whether or not it is able to detect antibodies in blood samples from patients who have been confirmed to have COVID-19 with a nucleic acid amplification test.” Specificity is the probability that a test correctly classifies uninfected samples as lacking antibodies for SARS-CoV-2. Similarly, the specificity of a test refers to its “ability to identify those without antibodies to SARS-CoV-2” and
is “estimated by testing large numbers of samples collected and frozen before SARS-CoV-2 is known to have circulated.” Sensitivity and specificity are pretest quantities, or validation metrics primarily meaningful before a serology test is taken. Sensitivity and specificity are defined by Supplementary Eqs. (3) and (4) in the Supplementary Information. In this article, we will use these definitions unless specified otherwise.

Rather, people who confront serology tests are likely interested in post-test probabilities, including positive predictive value (PPV) and negative predictive value (NPV). PPV is the probability that a person with a positive serology test indeed has a prior infection with and antibodies for SARS-CoV-2. NPV is the probability that a person who tests negative lacks antibodies for and has not yet been infected with SARS-CoV-2. Definitions and calculations for NPV and PPV are in the Supplementary Information. PPV and NPV are more relevant to patients and clinicians in interpreting serology test results than sensitivity and specificity.

The complements of the predictive values are probabilities that test results of each type are false. The False Positive Rate (FPR), the complement of PPV, is the proportion of people who test positive that are actually lacking a prior coronavirus infection. Similarly, the false negative rate (FNR), the complement of NPV, is the proportion of people who test negative that actually had a prior infection with coronavirus. The FPR (FNR) can be interpreted as the proportion of positive (negative) serology tests are false positives (negatives). Equations for FPR and FNR are provided in the Supplementary Information.

**Results**

This section reports values for the statistics described in “Background” to help contextualize serology test results. Prevalence estimates are reported in “Prevalence estimates”. Graphical displays of NPV and PPV for the range of values under study are found in “General interpretation in the context of antibodies testing”. Sensitivity, specificity, PPV, and FPR for tests under study are reported in “Analysis of individual antibodies tests”.

**Prevalence estimates.** Due to the lack of available diagnostic tests in the US, official counts of Covid-19 cases are likely undercounted\(^3\).\(^3\) Additionally, people with asymptomatic infections are unlikely to seek medical care or diagnostic testing and are likely excluded from official counts. Consequently, reliable prevalence estimates are limited. Prevalence, which affects predictive value estimates, can be considered unknown, and varies over time.

Emerging research is beginning to estimate population prevalence. Over the period from March 31 to April 7, by one estimate\(^3\), the prevalence by state ranged from about 0.4% in Alaska, Hawaii, Kentucky, and West Virginia to 8.5% in New York with a median prevalence of 0.9%. Another estimate\(^3\) from April 11 found infection proportions within states spanning from 0.1% in rural states to 7.0% in New York, and an overall US prevalence of 1.2%. A third group proposes a method\(^2\) with estimates that could indicate a prevalence of up to 10% of the population as of April 4, 2020. A collection of case studies is highlighted in “Application to specific locations”. In brief, the prevalence of Covid-19 in specific cities, states, and counties estimates during the early stage of the pandemic in the spring of 2020 ranged from less than 1% to about 30% in especially hard hit areas, such as Boston and New York City. According to more recent estimates as of September 2020 by the US Centers for Disease Control and Prevention\(^2\), most states had seroprevalence estimates ranging from 1% to 10%. As of the writing of this paper, only four states have estimates below 1% and five have estimates exceeding 10%.

**General interpretation in the context of antibodies testing.** In this section we investigate ranges of plausible values of sensitivity, specificity for antibodies tests available and and prevalence for relevant areas and compare the predictive values. Predictive values are of interest based on minima of 80% sensitivity and 90% specificity to reflect reported values for FDA-authorized serology tests and described in “Analysis of individual antibodies tests”. In general, the false negative rate is low and false positive rate is highly variable for available serology tests.

Figure 1 is a plot of NPV for these specificity, and sensitivity values and prevalence ranging from 1 to 30%, the range currently reported elsewhere as discussed in “Prevalence estimates” and “Application to specific locations”. Under these scenarios, the minimum NPV was 93.3%, indicating that the false negative rate was less than 10% in all scenarios. Thus, NPV should be high, and FNR should be low for all serology tests within similar ranges for sensitivity, specificity, and prevalence. In other words, negative serology tests have a high likelihood of accurately reflecting a lack of antibodies in the general population of non-infected individuals.

By contrast, Fig. 2 shows a corresponding plot spanning a wide range of plausible PPV values. PPV increases with prevalence and is low with lower rates of antibodies in the population. At fixed prevalence values, specificity also quickly increases PPV with prevalence. Higher sensitivity improves PPV, although the growth of PPV with prevalence and is low with lower rates of antibodies in the population. At fixed prevalence values, specificity also quickly increases PPV with prevalence. Higher sensitivity improves PPV, although the growth of PPV with prevalence and is low with lower rates of antibodies in the population. At fixed prevalence values, specificity also quickly increases PPV with prevalence. Higher sensitivity improves PPV, although the growth of PPV with prevalence and is low with lower rates of antibodies in the population.

**Analysis of individual antibodies tests.** As of May 22, 2020, the FDA had allowed 13 serology tests to operate under an Emergency Use Authorization (EUA)\(^3\). By November 24, 2020, the total number of tests with EUA had increased\(^3\) to 89, and EUA had been revoked for two prior tests. However, some of the updated results
are repetitive, with many companies reporting test characteristics for IgG, IgM, and Combined (IgG/IgM). In these cases, to balance space and conciseness with completeness, we reported the combined tests only. Characteristics of these 61 distinct tests appear in Table 1. Sensitivity estimates range from about 88% to 100%, with 95% confidence limits ranging from about 74% to 100%. Specificity estimates range from about 95% to 100%, with confidence bounds ranging from 88% to 100%.

**Figure 1.** Plot of NPV by prevalence (0–0.3), specificity (0.9–1), and sensitivity (0.8–1). The bar on the right with sensitivity is denoted by color, with lighter colors denoting lower sensitivity and darker colors denoting higher sensitivity. All parameters are reported as decimals ranging from 0 to 1. NPV values exceeded 0.9 for all input parameters.

**Figure 2.** Plot of PPV by prevalence (0.01–0.3), specificity (0.9–1), and sensitivity (0.8–1). Sensitivity is denoted by color, with lighter colors denoting low sensitivity and darker colors denoting higher sensitivity. All parameters are reported as decimals ranging from 0 to 1. PPV varied widely based on different parameters, ranging from 0.07 to 1.
| Test          | Type   | Sensitivity | Specificity | n (sen, spec) | FPR 1%     | FPR 5%     | FPR 10%     |
|--------------|--------|-------------|-------------|---------------|------------|------------|-------------|
| Abbott-Al    | G      | 100.0       | 99.9        | 34; 100       | 49.7       | 16.0       | 8.3         |
| Abbott-Ar    | G      | 100.0       | 99.6        | 88; 1070      | 28.4       | 7.1        | 3.5         |
| Abbott-AdvDxAl | M     | 95.0       | 99.6        | 40; 2985      | 29.4       | 7.4        | 3.7         |
| Abbott-AdvDxAr | M     | 95.0       | 99.6        | 40; 2965      | 29.4       | 7.4        | 3.7         |
| AccessBio    | C      | 98.4       | 98.9        | 64; 182       | 52.5       | 17.5       | 9.1         |
| AssureTech   | C      | 100.0       | 98.8        | 30; 80        | 54.3       | 18.6       | 9.7         |
| Babson       | G      | 100.0       | 100.0       | 29; 100       | 0.0        | 0.0        | 0.0         |
| BeckmanCoulter | G    | 96.8       | 99.6        | 95; 1400      | 29.0       | 7.3        | 3.6         |
| BeckmanCoulter | M    | 96.7       | 99.9        | 151; 1400     | 9.3        | 1.9        | 0.9         |
| Beijing W ELISA | P    | 96.7       | 97.5        | 30; 80        | 71.9       | 32.9       | 18.9        |
| Beijing W Rapid | P    | 100.0      | 98.8        | 30; 80        | 54.3       | 18.6       | 9.7         |
| Bio-Rad      | P      | 98.0       | 99.3        | 50; 600       | 41.4       | 11.9       | 6.0         |
| BioCan       | C      | 93.3       | 96.2        | 30; 79        | 80.1       | 43.6       | 26.8        |
| BioCheck     | C      | 99.1       | 97.2        | 110; 143      | 73.7       | 34.9       | 20.3        |
| Biohitt      | C      | 96.7       | 95.0        | 30; 80        | 83.7       | 49.6       | 31.8        |
| BioMerieux   | G      | 100.0      | 99.9        | 29; 989       | 9.0        | 1.9        | 0.9         |
| BioMerieux   | M      | 100.0      | 99.4        | 23; 308       | 37.3       | 10.2       | 5.1         |
| Collex       | C      | 93.8       | 96.0        | 128; 250      | 80.8       | 44.8       | 27.7        |
| DiaSorin     | G      | 97.6       | 99.3        | 41; 1090      | 41.5       | 12.0       | 6.1         |
| DiaSorin     | M      | 91.8       | 99.3        | 122; 2473     | 43.0       | 12.7       | 6.4         |
| Diazyme      | G      | 100.0      | 97.4        | 29; 852       | 72.0       | 33.1       | 19.0        |
| Diazyme      | M      | 94.4       | 98.3        | 108; 302      | 64.1       | 25.5       | 13.9        |
| Emory        | G      | 100.0      | 96.4        | 30; 638       | 78.1       | 40.6       | 24.5        |
| EUROMMUN     | G      | 90.0       | 95.0        | 30; 80        | 0.0        | 0.0        | 0.0         |
| Genalyte     | P      | 96.1       | 97.7        | 181; 862      | 70.3       | 31.3       | 17.7        |
| GenScript     | P      | 100.0      | 95.8        | 26; 88        | 0.0        | 0.0        | 0.0         |
| HangzhouRapid | C     | 100.0      | 95.4        | 30; 80        | 0.0        | 0.0        | 0.0         |
| HangzhouLaihe | C     | 100.0      | 98.8        | 30; 80        | 54.3       | 18.6       | 9.7         |
| Healgen      | C      | 100.0      | 97.5        | 30; 80        | 71.2       | 32.2       | 18.4        |
| InBios       | G      | 100.0      | 95.4        | 30; 80        | 0.0        | 0.0        | 0.0         |
| InBios       | M      | 96.7       | 98.3        | 30; 80        | 55.1       | 19.1       | 10.0        |
| JiangSu      | C      | 100.0      | 94.8        | 58; 97        | 87.3       | 49.7       | 31.9        |
| Luminex      | G      | 96.3       | 99.3        | 82; 603       | 41.8       | 12.1       | 6.1         |
| Megna        | C      | 100.0      | 95.0        | 30; 80        | 83.2       | 48.7       | 31.0        |
| Mt Sinai     | C      | 92.5       | 95.0        | 40; 74        | 0.0        | 0.0        | 0.0         |
| NanoEnTec    | C      | 96.7       | 98.8        | 30; 80        | 55.1       | 19.1       | 10.0        |
| Nirmidas     | M      | 93.1       | 97.9        | 58; 97        | 69.1       | 30.0       | 16.9        |
| Nirmidas     | G      | 87.9       | 97.9        | 58; 97        | 68.3       | 29.2       | 16.4        |
| Ortho-Clinical | G     | 90.0       | 99.1        | 40; 407       | 0.0        | 0.0        | 0.0         |
| Ortho-Clinical | P     | 100.0      | 99.0        | 49; 400       | 0.0        | 0.0        | 0.0         |
| QuanSys      | G      | 95.5       | 99.7        | 22; 585       | 23.7       | 5.6        | 2.7         |

Continued
Results for all tests improve with prevalence, but overall false positive rates remain concerning. Although only nine point estimates for false positive rates exceed 20% assuming 10% prevalence, which is higher than most currently estimated infection rates, the upper bound for false positive rates exceed 20% for 39 out of 61 tests. Moreover, only 15 (25%) tests from six companies—Abbott (3 of 4 minus Alinity IgG, Ortho-clinical (IgG and Pan Ig), Siemens (all 6 varieties), BeckmanCoulter (IgG and IgM), BioMerieux (IgG) and Roche—have upper limits of false positive rates below 10% when the prevalence is 10%. In other words, 46 out of 61 tests could reasonably produce at least 1 false positive out of 10 positive tests if the regional prevalence is 10%. Estimates or confidence bounds of exactly 100%, reported for many, are shown for completeness. These figures illustrate the known relationship that PPV should be lower in populations with lower prevalence and that PPV increases more rapidly for the remaining 50 tests are provided in the Supplementary Information. The figures highlight the relationship between PPV and prevalence for each of the 11 serology tests granted an EUA by the US FDA in the spring of 2020 that retained approval in November 2020. Similar figures for the remaining 50 tests are provided in the Supplementary Information. Figures 3 and 4 highlight the relationship between PPV and prevalence for each of the 11 serology tests granted an EUA by the US FDA in the spring of 2020 that retained approval in November 2020. Similar figures for the remaining 50 tests are provided in the Supplementary Information. The figures illustrate the known relationship that PPV should be lower in populations with lower prevalence, and that PPV increases more rapidly with increasing specificity than with increasing sensitivity.

### Table 1. Statistics for FDA authorized serology tests with EUA. All numbers are percentages. Interval estimates for sensitivity and specificity are 95% confidence intervals reported by the FDA. Interval estimates for the false positive rates are minimum and maximum values of all possible false positive rates calculated at the specified prevalence level for the corresponding test based on all possible estimates of sensitivity and specificity within the 95% confidence intervals. n refers to the number of samples used to calculate the pretest probabilities. The number on the right refers to the number of control samples used to estimate specificity. Test types are shortened as followed. "G" denotes IgG, "M" denotes IgM, "C" denotes combined IgG/IgM, and “P” denotes Pan-IgG.

| Test Type | Sensitivity | Specificity | n (sen, spec) | FPR 1% | FPR 5% | FPR 10% |
|-----------|-------------|-------------|---------------|--------|--------|--------|
| Quotient C | 93.0 (85.6, 96.8) | 99.8 (96.8, 100.0) | 86; 408 | 17.6 (0.0, 61.8) | 3.9 (0.0, 23.7) | 1.9 (0.0, 12.8) |
| Roche C   | 100.0 (88.3, 100.0) | 99.8 (99.7, 99.9) | 29; 5272 | 16.5 (9.0, 25.2) | 3.7 (1.9, 6.1) | 1.8 (0.9, 3.0) |
| Salofa C  | 93.3 (78.7, 98.2) | 98.8 (93.3, 99.8) | 30; 80 | 56.0 (16.8, 89.4) | 19.6 (3.7, 61.8) | 10.4 (1.8, 43.4) |
| Shenzhen C| 100.0 (97.4, 100.0) | 98.7 (96.2, 99.5) | 142; 226 | 56.3 (33.1, 79.4) | 19.8 (8.7, 42.6) | 10.5 (4.3, 26.0) |
| SiemensADVIA G | 100.0 (91.6, 100.0) | 99.9 (99.4, 99.9) | 42; 1831 | 9.0 (9.0, 30.2) | 1.9 (1.9, 7.7) | 0.9 (0.9, 3.8) |
| SiemensADVIA P | 100.0 (92.4, 100.0) | 99.8 (94.4, 99.9) | 47; 1589 | 16.5 (9.0, 39.1) | 3.7 (1.9, 11.0) | 1.8 (0.9, 5.5) |
| SiemensAtellica G | 100.0 (91.6, 100.0) | 99.9 (99.7, 100.0) | 42; 1841 | 9.0 (0.0, 24.5) | 1.9 (0.0, 5.9) | 0.9 (0.0, 2.9) |
| SiemensAtellica P | 100.0 (91.6, 100.0) | 99.8 (99.3, 99.9) | 42; 1091 | 16.5 (9.0, 43.1) | 3.7 (1.9, 12.7) | 1.8 (0.9, 6.4) |
| SiemensDimEXL P | 100.0 (95.4, 100.0) | 99.9 (99.5, 100.0) | 79; 1529 | 9.0 (0.0, 34.2) | 1.9 (0.0, 9.1) | 0.9 (0.0, 4.5) |
| SiemensDimVista P | 100.0 (95.4, 100.0) | 99.8 (99.4, 99.9) | 79; 1529 | 16.5 (9.0, 38.4) | 3.7 (1.9, 10.7) | 1.8 (0.9, 5.4) |
| Sugentech G | 96.7 (83.3, 99.4) | 100.0 (95.4, 100.0) | 30; 80 | 0.0 (0.0, 84.5) | 0.0 (0.0, 51.2) | 0.0 (0.0, 33.2) |
| TBG C | 93.3 (78.7, 98.2) | 95.0 (87.8, 98.0) | 30; 80 | 84.1 (66.8, 93.8) | 50.5 (27.9, 74.7) | 32.5 (15.5, 58.2) |
| ThermoFisher P | 96.7 (83.3, 99.4) | 97.5 (91.3, 99.3) | 30; 80 | 71.9 (41.1, 91.2) | 32.9 (11.8, 66.5) | 18.9 (6.0, 48.5) |
| UniVV A2 P | 97.5 (87.1, 99.6) | 99.1 (97.3, 99.7) | 40; 320 | 47.7 (23.0, 75.4) | 14.9 (5.4, 37.1) | 7.7 (2.6, 21.8) |
| Vibrant C | 98.1 (90.1, 99.7) | 98.6 (97.1, 99.3) | 53; 501 | 58.6 (41.0, 76.1) | 21.3 (11.8, 37.9) | 11.4 (5.9, 22.5) |
| Wadsworth P | 88.0 (80.5, 92.8) | 98.8 (97.3, 99.5) | 108; 433 | 57.4 (34.8, 76.9) | 20.6 (9.3, 38.9) | 10.9 (4.6, 23.2) |
| Xiamen C | 100.0 (88.7, 100.0) | 96.2 (89.5, 98.7) | 30; 80 | 79.0 (56.3, 92.1) | 41.9 (19.8, 69.2) | 25.5 (10.5, 51.6) |
| Zeus G | 93.3 (78.7, 98.2) | 100.0 (94.8, 100.0) | 30; 70 | 0.0 (0.0, 86.7) | 0.0 (0.0, 55.7) | 0.0 (0.0, 37.3) |

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*Abbreviations: IgG, IgM, Pan-Ig, and SARS-CoV-2 indicate IgG, IgM, Pan-IgG, and SARS-CoV-2 antibodies, respectively.*
were validated on samples of less than 100. Yet, as shown by the definitions and equations in the Supplementary Information, perfect (100%) specificity implies perfect PPV and perfect sensitivity implies perfect NPV. In these cases, it is especially important to consider the entire range of values for PPV and FPR. Indeed, while tests by Mt. Sinai and Euroimmun have point estimates and lower interval estimates of 0% false positives, upper interval estimates climb to about 86%. Even at 10% prevalence, if the true specificity is closer to the lower 95% confidence limit, then false positive rate of Euroimmun and Mt. Sinai would be above 35%, rendering over a third of positive serology test results as likely false positives.

The test by Roche pharmaceuticals, advertised as highly accurate36, indeed has high PPV and low false positive rates even at 1%, with an upper limits for the false positive rate of 25.2%. The Roche test is the only test available by the end of May 2020 that could have reasonably claimed to expect more true positive results than false positive results in populations with low prevalence (1% or less). However, it would have still been reasonable to expect that up to one quarter of positive test results could have come from patients lacking antibodies to SARS-COV-2. Given the sample size33 of 29 for calculating sensitivity, the associated uncertainty could be compounded in the estimates of PPV and FPR, rendering the upper bounds critical to measure and understand. Even 6 months later, only one test, (Simens Atellica IgG) has improved on this figure, with the smallest upper confidence limit for FPR of 24.5% at 1% prevalence and a corresponding FPR point estimate of about 9%.

Application to specific locations
In this section, we evaluate PPV and FPR for a set of areas with three local studies of seroprevalence, in California, New York, and Boston. When rigorous prevalence estimates are unavailable, we use the proportion of positive tests as surrogates for prevalence for the purpose of estimating the rates of false positives in these studies. Rationale for and limitations of this approach along with a sensitivity analysis are discussed in the Supplementary Information.

![Figure 3. PPV by prevalence (up to 10%) for FDA tests (a-d).](image-url)
Predictive values in the Santa Clara Study nearly spanned the entire range of probabilities. Using prevalence values reflecting prior estimates ranging from 0% to 5%, the PPV in Santa Clara County at the time of the study ranges from 0% to 96% (Fig. 5). Prevalence near the low but nonzero end of the updated estimates (e.g. 0.2%) correspond to PPV ranging from about 9.7% to 47.7%, indicating that between about 26 and 46 of the 50 positive tests could be false. For prevalence near the high end of the updated estimates (4.7%) ranges from 73.0% to 95.8%, or 2–14 false positives. Reanalyses estimate smaller upper bounds on prevalence (2.1% and 3.2%), which PPV ranges of 52.2%–92.3% or 63.9%–93.8%. These estimates correspond to false positive counts ranging from 2 to 24 or 3 to 18.

Santa Clara County. An early seroprevalence study was conducted in Santa Clara County. However, after extensive scrutiny, the authors provided updated estimates. Based on the updated preprint[37], the estimated prevalence adjusted for test performance characteristics were 1.2% (95% CI 0.7%–1.8%) unweighted and 2.8% (95% CI 1.3%–4.7%) for weighted estimates based on demographic characteristics in Santa Clara County. Reanalyses[38,39] reported updated seroprevalence ranges of 0.27% and 3.21% and 0%–2.1%. An estimate of prevalence in California from March 31 to April 7 is 0.9%[31]. Estimates of sensitivity and specificity vary[37–39]; we use the Bayesian posterior estimates[39] combining information from all sources as 99.5% specificity with a 95% posterior interval of (98.8%, 99.8%) and 81.8% sensitivity (64.2%, 91.0%).

On April 23, Governor Andrew Cuomo announced results from a serology study in New York[40]. Seropositivity rates were 13.9% for the state overall and differed by region. New York City, Long Island, Westchester, and Rockland, and elsewhere in New York, respectively, had 21.2%, 16.7%, 11.7%, and 3.6% seropositive. Specificity for the test was reported to be in the range of 93–100%[41], and sensitivity was not listed. However,
the test was attributed to Wadsworth Center by the New York State Department of Health; the Wadsworth test parameters are reported in Table 1. Results were then updated on May 2. At that time, 12.3% of the population of New York state was reported to have Covid-19 antibodies based on a test of 15,000 people. By region, these figures ranged from 1.2% seropositive in North Country to 19.9% in New York City. We estimate the PPV for all combinations of values reported in all of these sources assuming the same serology tests were used in both studies.

Figure 6 shows the range of PPV based on each of these possible values of sensitivity, specificity, and prevalence. New York City and Long Island had the highest prevalence and highest PPV, ranging from 74% to 98% and 60% to 97% in all scenarios. Statewide and other areas are in the middle: 60%–96% for Rockland, 65%–97% for statewide. By contrast, PPV can be as low as 30% for the rest of the state, assuming a prevalence of 3.6%, if the specificity is 93% or as high as 87% if sensitivity is at the upper limit of the confidence interval reported in the EUA. Even worse, areas with low prevalence such as North Country (1.2%), Central NY (1.9%), and Capital District (2.2%) had PPV estimates ranging from 12% to 69%, 18% to 78% and 21% to 81% in other words, the false positive rate in New York ranged from 2% to 88% depending on the region and assumed prevalence under consideration and uncertainty in the sensitivity and specificity.

Chelsea, Massachusetts. Researchers at Massachusetts General Hospital conducted a seroprevalence study in the city of Chelsea and reported that 31.5% of participants tested positive. The researchers on the Chelsea study reported specificity exceeding 99.5%. However, the manufacturer, BioMedomics, which is not part of the labs with EUA in “Analysis of individual antibodies tests”, reports a sensitivity of 88.66% and specificity of 90.63%.

Assuming prevalence of 31.5% and specificity and sensitivity values reported by BioMedomics, PPV was only about 81%. This means that in this sample of 63 positives, about 51 are expected to be true positives and about 12 are expected to be false positives. Thus, the prevalence estimate in Chelsea reported in the press based on this sample alone is likely to be too high. In addition, participants were recruited by a convenience sample of people outside on a particular street, which may not be representative of the general population in Chelsea.

Discussion
Antibodies tests can yield two possible errors with different implications. Consequences of false negative test results would likely relate to failing to remove negative effects of limitations during the pandemic. For example, assuming that antibodies indeed confirm protection, then people with antibodies who test negative would be safe to return to work but their negative test might convince them to remain at home. This would prolong the...
negative mental and physical effects of social isolation as well as economic effects to individuals and society overall. Fortunately, the false negative rate was under 10% in all scenarios.

Unfortunately, the false positive rate can be shockingly high. Based on the prevalence estimated throughout the US and serology studies in California, New York and Boston, the FPR of antibody test results range from 2% to 88%. Point estimates of tests with an EUA reached 86% and upper limits reached 93% when the prevalence is 1%. Tests with low PPV and high FPR can be dangerous by giving patients with positive tests a false sense of security. Ironically, these people may then increase their risk of contracting Covid-19 if they relax their use of protective measures, such as mask wearing and social distancing.

The timing of the test may impact the result, as discussed in the Supplementary Information. Briefly, seroconversion is the process during which antibodies develop after infected by Covid-19 become detectable in the blood; the seroconversion duration could complicate the consideration of interpretation of serology test results. After infection, patients took about 3–40 days to develop detectable antibodies. Typically, after 14 days, most patients will develop antibodies. If the testing period is within 14 days, the sensitivities of the tests will be lower.

The number and implication of false positives is growing with large organizations encouraging widespread serology testing. Quest Diagnostics is offering tests by Abbott, Ortho-Clinical and Euroimmun for purchase. The tests can have up to 84% FPR in locations with 1% prevalence. Even at 10% prevalence, over one-third of positives could be false. OneBlood, a non-profit blood donation and distribution organization, is encouraging large scale blood donation and then testing samples for antibodies using the OrthoClinical total test. As discussed in “Analysis of individual antibodies tests”, the OrthoClinical test could have a false positive rate of over 50% with 1% prevalence or nearly 10% if the prevalence is 10%. Further, OneBlood is planning to use blood samples testing positive for antibodies as convalescent plasma. In fact, on August 23, the FDA granted EUA for convalescent plasma in patients hospitalized with Covid-19. As shown in this paper, single serology tests of the general population in low prevalence areas could yield a large number of false positives, which could inadvertently harm patients. Using all samples that test positive could mean that large numbers of samples falsely considered to contain convalescent plasma which would become inadvertent placebos for patients actively struggling with Covid-19.

More recently, with the impending approval of vaccine candidates, there is a need to determine the prioritization of groups throughout the dose distribution process. In some discussions, patients who previously contracted covid-19 could be considered lower priority for receiving vaccine until after the uninfected public. Given the false positives discussed in serology tests in this paper, it would be imprudent to determine past disease status by widespread serology testing alone. In this case, uninfected individuals who falsely test positive on serology tests would be denied the vaccine in a timely manner and therefore would have to wait longer for the opportunity to vaccinate and protect themselves from the virus. We recommend against using single serology tests to screen for prior infection. In fact, the length of protection from reinfection is unknown for individuals with prior exposure either to the disease itself or via vaccination.

One recommendation for individuals who test positive is to consider a follow-up antibody test. For instance, if the FPR is 50%, assuming independent tests, the probability of two false positives drops in half (25%). The FDA includes a calculator for PPV of individual and combined tests. Follow-up tests are common in other diseases with low PPV screening methods, such as mammograms for breast cancer. For instance, one could use a highly sensitive test with sensitivity/specificity, say, 99% and 90%, respectively, as the initial test, and then followed up with a highly specific test with sensitivity/specificity of 90% and 99% respectively, as the second test. Then, the FPR (i.e., 1-PPV) would drop from 81.9% to 10% for a person with prevalence of 10%. For a person with prevalence of 1%, the FPR could drop from 47.6% to 1%. Another idea is to test all contacts for antibodies and use their results as evidence to support or refute the original serology test. Pursuing contacts of additional seropositive individuals may increase contact tracing and testing, which can either hinder growth of future outbreaks or divert scarce resources from higher risk contacts. Moreover, increased testing brings cost and feasibility concerns.

There are some additional limitations of our paper. For instance, some of the information may become outdated quickly. Tests operating under an FDA EUA will likely increase over time. For instance, Abbott Alinity was added to the original 12 tests made available by FDA under EUA in early May 2020 while writing the first draft of this paper. At the time, the FDA noted that at least 160 serology tests were available before the FDA increased its oversight. This implies some of the antibody tests on the market might even have lower sensitivity or specificity than those included in this paper and therefore have even higher FPR. Indeed, before the original paper submission in June 2020 and this revision in December 2020, two tests, AutoBio and ChemBio, had their FDA EUA revoked.

Conclusively, serology tests for the novel coronavirus generally have low false negative rates and highly volatile false positive rates. While false positive rates decrease with increasing prevalence, current prevalence estimates remain low in most areas of the US as of the writing of this manuscript. With increasing serology testing and likely increased reporting of testing results, it is critical to understand these values and interpret test results properly. We hope that this context and interpretation can aid doctors, patients, researchers, and policy makers in informed decision making, which may even save lives.
Methods
We collected reported sensitivity and specificity values of serology with EUA approval by the US FDA. Prevalence estimates were also collected to determine an appropriate range for the plots. These values were combined to produce estimates of PPV and NPV for a variety of input parameter values. We then honed in on specific FDA tests and areas that have conducted serology tests to provide estimates and uncertainty for PPV and false positive rates.

All programs utilized R version 3.6.1\(^{15}\). PPV and NPV were calculated using package MKmisc\(^{27}\). Plots were created with packages plotly\(^{18}\) and ggplot\(^{20}\). Figures 1 and 2, as higher dimensional plots, were designed to allow interactive visualization. Code to generate the plots and view them in an interactive mode may be downloaded from our github repository at https://github.com/nbrownst/AntibodiesPredictiveValues.

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Author contributions
N.C.B. created the code, figures and tables. Both authors (N.C.B and Y.A.C.) participated in the literature review and wrote and reviewed the manuscript.

Competing interests
Dr. Brownstein (NCB) served as an ad-hoc reviewer in 2020 for the American Cancer Society, for which she received sponsored travel during the review meeting and a stipend of $300. NCB received a series of small awards for conference and travel support, including $500 from the Statistical Consulting Section of the American Statistical Association for Best Paper Award at the 2019 Joint Statistical Meetings and the $500 Lee Travel Award from the Caucus for Women in Statistics to support attendance at the 2018 Joint Statistical Meetings. NCB also received a Michael Kutner/ASA Junior Faculty Travel Award of $946.60 to attend the 2018 Summer Research Conference of the Southern Regional Council on Statistics and travel support of $708.51 plus a registration waiver from the ASA Statistical Consulting Section for 2021-2023. YAC is a member of the International Society for Computational Biology and American Association for Cancer Research. Both authors are members of the ASA and serve on the SRC at Moffitt Cancer Center.

Additional information
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