Revisiting the distance to radio Loops I and IV using Gaia and radio/optical polarization data

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ABSTRACT

Galactic synchrotron emission exhibits large-angular-scale features known as radio spurs and loops. Determining the physical size of these structures is important for understanding the local interstellar structure and for modeling the Galactic magnetic field. However, the distance to these structures is either under debate or entirely unknown. We revisit a classical method of finding the location of radio spurs by comparing optical polarization angles with those of synchrotron emission as a function of distance. We consider three tracers of the magnetic field: stellar polarization, polarized synchrotron radio emission, and polarized thermal dust emission. We employ archival measurements of optical starlight polarization and Gaia distances, and construct a new map of polarized synchrotron emission from WMAP and Planck data. We confirm that synchrotron, dust emission, and stellar polarization angles all show a statistically significant alignment at high Galactic latitude. We obtain distance limits to three regions towards Loop I of 112±17 pc, 135±20 pc, and <105 pc. Our results strongly suggest that the polarized synchrotron emission towards the North Polar Spur at b > 30° is local. This is consistent with the conclusions of earlier work based on stellar polarization and extinction, but in stark contrast with the Galactic center origin recently revisited on the basis of X-ray data. We also obtain a distance measurement towards part of Loop IV (180±15 pc) and find evidence that its synchrotron emission arises from chance overlap of structures located at different distances. Future optical polarization surveys will allow the expansion of this analysis to other radio spurs.

Keywords: ISM: magnetic fields — ISM: structure — Galaxy: local interstellar matter — polarization

1. INTRODUCTION

The low frequency (≲70 GHz) radio sky at high Galactic latitudes is dominated by bright, well-known, large-scale features (Berkhuijsen et al. 1971). They have steep radio spectra and are highly polarized, indicative of synchrotron radiation (for determinations of the spectral indices see Vidal et al. 2015; Planck Collaboration et al. 2016a). Some of these features appear to trace full or partial circles on the sky, and are referred to as ‘loops’ or ‘arcs’. The term ‘spurs’, introduced by Berkhuijsen et al. (1971), is used to describe continuous regions of bright synchrotron intensity that do not necessarily trace circles. As early as their discovery, it was recognized that the structures are likely in the Galactic neighborhood of the Sun, which explains their large (tens of degrees) angular sizes. The common assumption on the origin of these structures is that they are the remnants of one, or a series of supernova explosions (for a review see Salter 1983).

Understanding these large-scale objects is important for a number of reasons. They are physical structures that are likely nearby and are therefore an important component for understanding the local interstellar environment. If indeed they are old supernova remnants, they trace historical star-formation events that occurred in the vicinity of the Sun (within the nearest kiloparsec). They also allow the detailed study of such objects
before they fade into the general background due to radiative cooling (e.g., Sarbadhicary et al. 2017, and references therein). Measuring the large-scale magnetic field (henceforth, B-field) of our Galaxy is a major endeavour that is important for understanding the Galactic dynamo and the structure of the Galactic disk (Planck Collaboration et al. 2016b). Whether nearby or distant, radio spurs and their local B-fields can cause confusion for studies attempting to characterize the large-scale Galactic B-field (e.g., Jaffe 2019). Furthermore, modeling the emission of these structures could be important for understanding and removing polarized foreground emission from sensitive Cosmic Microwave Background (CMB) surveys (e.g., Dunkley et al. 2009; Remazeilles et al. 2018).

The physical locations of most of these features are either debated between the proponents of rival interpretations or entirely unknown. A prominent example is the North Polar Spur (NPS), which is the brightest part of the larger Loop I, rising vertically above the Galactic plane at a longitude of \( \sim 30^\circ \) and having a diameter of \( \sim 100^\circ \) on the sky (Large et al. 1962; Berkhuijsen et al. 1971). Soon after its discovery, Bingham (1967) found that the electric vector position angles (polarization angles) of a small number (\( \approx 10 \)) of stars were aligned with the B-field direction traced by synchrotron polarization, thus suggesting a distance of \( \sim 100 \) pc to the high-latitude part of Loop I. Subsequent studies of the optical polarization have confirmed this conclusion (Spoelstra 1972; Ellis & Axon 1978; Leroy 1999; Santos et al. 2011; Berdyugin et al. 2014), and are in agreement with the distance to the neutral gas likely associated with the NPS (Puspitarini & Lallement 2012; Das et al. 2020). In apparent contradiction with these determinations, an alternative model has been proposed for Loop I, in which the structure is located at the Galactic center and forms part of a bipolar hyper-bubble extending out to the Galactic halo (Sofue 1977, 2000). In partial support of this model, the absorption of X-rays associated with the NPS necessitates a much larger distance than 100 pc (300–4 kpc; Sofue 2015; Lallement et al. 2016). Recently, several studies of X-ray data have argued in favor of the NPS being at the Galactic centre at 7.8 kpc (Akita et al. 2018; Predehl et al. 2020; Kataoka et al. 2021), possibly related to the Fermi \( \gamma \)-ray bubbles (Dobler et al. 2010). The debate has been reviewed several times in the past few years (Planck Collaboration et al. 2016a; Dickinson 2018; Kataoka et al. 2018).

With the influx of new data on the Galactic B-field we can hope to gain better insights on these interesting radio features and their relation to the B-field on large scales (e.g., Planck Collaboration et al. 2016b). New maps of polarized synchrotron and thermal dust emission (Bennett et al. 2013; Planck Collaboration et al. 2020a) and stellar polarization surveys (e.g., Berdyugin et al. 2014; Clemens et al. 2020) can provide measurements of the B-field geometry with unprecedented detail (see Section 2). In conjunction with the B-field tracers, we can use stellar distance measurements from Gaia (Gaia Collaboration et al. 2016).

The basis of the method for placing distance limits to synchrotron spurs is to search for alignment between stellar and synchrotron polarization angles. Alignment can be achieved under certain circumstances. First, the synchrotron polarization along a line of sight is dominated by the emission local to the spur (i.e., there is no significant confusion from background/foreground emission), and Faraday rotation is negligible (the latter is true far from the Galactic plane at frequencies higher than 10 GHz). If this is the case, the intrinsic synchrotron polarization angles at emission trace the magnetic field geometry local to the spur. For the brightest spurs (e.g., Loop I) this is likely the case, as the polarization angles are closely aligned with the axis of the structure (Vidal et al. 2015). Second, if the synchrotron spurs are indeed the result of B-fields that have been compressed along the surface of an evacuated cavity (by a supernova explosion e.g., Ferriere et al. 1991), then it is likely that dust will also remain on the surface. The dust grains induce polarization to light from background stars. Since starlight polarization is an integrated effect of dust along the line-of-sight to the star; the dust that is colocated with the synchrotron emission will give rise to stellar polarization that traces the same B-field probed by the synchrotron emission. Thus a significant correlation between stellar and synchrotron polarization angles allows us to infer that the synchrotron emission is closer than the stars that show the correlation.

By using many stars in a given region of sky, and looking for alignment of their polarization angles with the B-field orientation inferred from synchrotron/dust emission data, we can statistically infer a distance to the synchrotron spurs (as originally done by Bingham 1967; Spoelstra 1972). Of course, the conditions for alignment may not be met. An alternative hypothesis can also be tested: if the B-field orientations are not aligned in a given region, then the synchrotron and thermal dust emitting ISM must be at different distances.

In this paper we revisit the comparison between the polarization of starlight and synchrotron emission, aiming to improve the existing distance determination towards synchrotron loops and spurs. Our analysis brings together a recently compiled catalog of stellar polarization measurements, as well as improved synchrotron
data obtained by combining WMAP and Planck low frequency maps. We make use of three additional datasets: (a) accurate stellar distances from the Gaia mission, (b) the latest Planck polarized dust emission map and (c) 3D maps of the stellar extinction in the Solar neighborhood. We introduce the data and pre-processing in Section 2. The comparison between the three different polarization datasets is presented in Section 3. We determine the distance to two structures: Loop I and Loop IV in Sections 3.2, 3.3 and 3.4. We discuss our findings in Section 4 and conclude in Section 5.

2. DATA & PRE-PROCESSING

2.1. Polarized synchrotron emission

Synchrotron radiation is produced by relativistic electrons spiralling in a magnetic field. If the field is regular and ordered, the polarization fraction can be as high as \( \approx 75\% \) (Rybicki & Lightman 1985). The measured polarization angle traces the magnetic field orientation projected on the sky. If there is no depolarization (e.g., along the line-of-sight) then this provides a direct way of measuring the orientation of the B-field.

At frequencies of a few GHz and higher, the radiation is optically thin and has a steep spectrum falling with frequency (with a brightness temperature spectral index \( \beta \), of \( \approx -3 \); Bennett et al. 2013; Planck Collaboration et al. 2016a). Thus low frequencies (\( \lesssim 1 \) GHz) would provide a very bright signal. However, at frequencies below a few GHz, the polarization angle is rotated under the effect of Faraday Rotation (e.g., Wolleben et al. 2006; Carretti et al. 2019; Hutschenreuter & Enßlin 2020). This can depolarize the observed signal and means that the angle is no longer perpendicular to the B-field.

Fortunately, WMAP (Bennett et al. 2013) and Planck (Planck Collaboration et al. 2020a) have mapped the entire sky at frequencies above 20 GHz in intensity and polarization. At these frequencies, Faraday Rotation is negligible (\( \ll 1^\circ \) rotation) except for regions near the Galactic Centre (Vidal et al. 2015). The main limitation with these data is the low signal-to-noise ratio (S/N), particularly in areas of the sky where there is little polarized synchrotron emission. The lowest frequency channels of these two surveys provide the highest S/N; WMAP K-band at 22.8 GHz and Planck LFI at 28.4 GHz.

To increase the S/N, we can smooth and degrade the maps to a lower angular resolution. However, even after smoothing there remain large areas of the sky where the S/N is very low. To increase the S/N further, we combine the three lowest channels of WMAP (22.8, 33.0 and 40.7 GHz) with Planck data at 28.4 and 44.1 GHz (for more details see Peel et al., in prep., which follows a similar technique to Planck Collaboration et al. 2016a). We use the Stokes \( Q,U \) maps, which are provided in HEALPix format (Górski et al. 2005) on the Planck Legacy Archive\(^1\). We first smooth the \( Q,U \) maps to a common \( 1^\circ \) angular resolution, using the published beam window functions, and degrade to a given HEALPix \( N_{\text{side}} \). We then include color corrections and extrapolate each pixel to a common frequency of 28.4 GHz assuming a spectral index \( \beta = -3.1 \). This is the average value measured at these frequencies and does not appear to vary much across the sky (Bennett et al. 2013; Fuskeland et al. 2021), except for possibly a few areas near the Galactic plane (Planck Collaboration et al. 2013). We then make the weighted average of these data (see also Planck Collaboration et al. 2016a), based on the noise covariance matrices computed using Monte Carlo noise realizations. The noise realizations make use of the published \( QQ \), \( QU \) and \( UU \) variance maps, with each realization smoothed to \( 1^\circ \) before combining to calculate the smoothed covariance matrices at a given \( N_{\text{side}} \) (similarly to Planck Collaboration et al. 2013a, see Peel et al., in prep.). The majority of the weight comes from WMAP 22.8 GHz, with some regions dominated by Planck 28.4 GHz. Nevertheless, there is an improvement in the S/N of \( \approx 2 \) on average.

Fig. 1 shows the polarized intensity at 28.4 GHz at a resolution parameter of \( N_{\text{side}} = 32 \) (pixels \( \approx 1.8 \) on a side). Pixels with S/N < 4, corresponding to an angle uncertainty of \( \sigma_\phi > 7^\circ \), have been masked and are not used (see Section 2.4). The bright loops and spurs seen in the map are detected at high significance.

2.2. Polarized thermal dust emission

Thermal dust emission from cold dust (\( T \sim 10–100 \) K) dominates the continuum at frequencies higher than \( \sim 300 \) GHz (Planck Collaboration et al. 2014). Polarized emission arises from non-spherical dust grains aligning their short axis with the B-field. Thus, as in synchrotron emission, the polarization angle is perpendicular to the B-field. Planck has mapped the polarized thermal dust emission at frequencies 100–353 GHz with the HFI instrument (Planck Collaboration et al. 2015a). The highest frequency (353 GHz) has the highest signal-to-noise ratio due to the steeply rising spectrum of thermal dust emission.

For our analysis we use the CIB-filtered common resolution map at 353 GHz (Planck Collaboration et al. 2020b,c), which provides the maximum signal-to-noise ratio.

\(^1\) https://pla.esac.esa.int/pla/
ratio. We mask pixels with S/N < 4 and apply the same degradation as for the synchrotron map to a common N_{side}.

2.3. Starlight polarization catalog

We use a new compilation of optical polarization data (Panopoulou et al., in prep.). The catalog contains ∼35,000 stars with measured polarization. The data cover a wide range of environments, from molecular clouds to the diffuse, high Galactic-latitude ISM. Quantities in the catalog include: stellar polarization fraction, p, polarization angle in Galactic coordinates, \( \theta^* \), and associated uncertainties. The catalog also provides a cross-match with Gaia DR2 (Gaia Collaboration 2018). Distances are obtained from Bailer-Jones et al. (2018), and include a point estimate as well as 68% confidence intervals. For stars that are not included in Gaia DR2, or do not have distance estimates in Bailer-Jones et al. (2018), distances were obtained by inverting the Hipparcos parallax, where available. We discard any entries in the catalog where the polarization angle uncertainty, \( \sigma_{\theta^*} \), is not provided. We convert all polarization angles to the range \([-90^\circ, 90^\circ]\). If there are multiple measurements of the same star (matching coordinates to within a radius of 1-arcsecond), we use the measurement with smallest uncertainty in polarization angle.

For comparison with the polarization angles in emission, we bin the data into HEALPix maps of \( N_{\text{side}} = 32 \) (1.8'). Within each HEALPix pixel, we calculate the weighted mean polarization angle, \( \theta \), of the \( N \) stars in the pixel:

\[
\theta = \frac{1}{2} \arctan \left( \frac{\frac{1}{W} \sum_{i=1}^{N} w_i \sin(2\theta^*_i), \frac{1}{W} \sum_{i=1}^{N} w_i \cos(2\theta^*_i)}{1 \sum_{i=1}^{N} w_i} \right),
\]

as appropriate for circular quantities (e.g., Fisher 1995), where \( \arctan \) is the two-argument arctangent function. The weights are: \( w_i = (\sigma_{\theta^*_i})^{-2} \) and \( W \) is the sum of the weights, \( \sum_{i=1}^{N} w_i \). For stars with very large uncertainties, i.e. \( \sigma_{\theta^*} > 45^\circ \), we assign a weight of 0. To avoid assigning excessively large weights to stars with \( \sigma_{\theta^*} < 1^\circ \), we set a minimum uncertainty of 1° to these stars. This limit also reflects a systematic uncertainty in the absolute calibration of the polarization angle, which arises from the intrinsic variability of calibrator stars (Ramaprakash et al. 2019).

Throughout the text, we use the symbol \( \theta^* \) to denote the polarization angle of an individual star. We use the symbol \( \theta \) to denote the polarization angle of stars averaged within a sky pixel as described above. All angles are in Galactic coordinates, measured according to the IAU convention from Galactic North through East.
2.4. Angle differences

Our analysis makes use of polarization data from three different tracers of the magnetic field: dust emission, synchrotron emission, and starlight absorption. While starlight polarization angles are parallel to the magnetic field, those of synchrotron and dust emission are perpendicular to it. We rotate the polarization angles of the synchrotron, $\phi_{\text{synch}}$, and dust emission, $\chi_{\text{dust}}$, by 90° for the entirety of the analysis:

$$\phi_{\text{synch}} = \frac{1}{2} \arctan(-U_{\text{synch}}, Q_{\text{synch}}) - 90^\circ$$  \hspace{1cm} (2)

$$\chi_{\text{dust}} = \frac{1}{2} \arctan(-U_{\text{dust}}, Q_{\text{dust}}) - 90^\circ$$  \hspace{1cm} (3)

where $\arctan$ is the two-argument arctangent function, while $U_{\text{synch}}, Q_{\text{synch}}$ and $U_{\text{dust}}, Q_{\text{dust}}$ are the Stokes parameters of the synchrotron and dust emission maps (Sections 2.1, 2.2), respectively. We have multiplied the Stokes parameter $U$ by -1 to convert from the COSMO convention to IAU (e.g., Planck Collaboration et al. 2020b). We transform each angle $\psi'$ by:

$$\psi = (\psi' + 90^\circ) \mod(180^\circ) - 90^\circ,$$  \hspace{1cm} (4)

so that the final angle $\psi$ is defined in the range $[-90^\circ, 90^\circ]$. We make use of the following angle differences between the three magnetic field tracers: $\theta^* - \phi_{\text{synch}}, \theta^* - \chi_{\text{dust}},$ and $\chi_{\text{dust}} - \phi_{\text{synch}}$.

We wish to study regions where we can be confident of the alignment between different magnetic field tracers. For this reason, we apply a S/N threshold on the polarized intensity of synchrotron emission and dust emission of $S/N > 4$, which corresponds to an uncertainty in the polarization angle of $7^\circ$. Thus we mask any regions in our maps with $S/N$ lower than this threshold.

We aim to use the observed alignment between the three $B$-field tracers to constrain our estimates of the distance to a synchrotron spur. However, if the synchrotron emission has significant contributions from background or foreground components along the line-of-sight, then the observed synchrotron polarization angle may not represent the $B$-field orientation local to the spur, depending on the relative brightness of each component. For a foreground or background component whose polarized intensity is 60% that of the synchrotron spur, the maximum angle difference between the observed polarization angle and that of the $B$-field at the spur’s location is 20°. We exclude potentially problematic situations by requiring that the observed offset between the synchrotron $\phi_{\text{synch}}$ and any other tracer be $< 20^\circ$. Furthermore, our analysis is focused on the brightest polarized radio emission from the loops/spurs, thus reducing the possibility of bias due to foreground or background emission. Nevertheless, chance alignments can still occur; for a random distribution of angle differences, there is a 22% probability that any one measurement is within $< 20^\circ$. However, since we are dealing with multiple (tens of) stellar measurements within a given region, chance alignments are much less likely (of order a few %).

To quantify the significance of the alignment between two angles, we use the Projected Rayleigh Statistic (PRS, Jow et al. 2018), which is specifically designed for dealing with orientations rather than circular quantities. The PRS is an optimal statistic for testing the hypothesis that a distribution of angle differences is consistent with alignment. We use the definition of the PRS that takes into account measurement uncertainties:

$$\text{PRS} = \frac{1}{\sqrt{\sum_i w_i^2}} \sum_i w_i \cos 2\Delta\psi_i,$$  \hspace{1cm} (5)

where $\Delta\psi_i$ is the difference between two polarization angle measurements (e.g., $\theta^* - \phi_{\text{synch}}$) and $w_i$ is the weight as defined for equation 1. The derived PRS will be compared to the PRS of a uniform distribution of angle differences in Section 3.4.

2.5. Extinction maps

We use the Leike et al. (2020) map of 3D dust extinction to measure the distribution of interstellar dust as a function of distance. We query the map via the dustmaps Python package (Green 2018) and obtain the mean value of $Gaia$ G band optical depth per parsec, $\tau_G$/pc, in each voxel along a line of sight. We convert the native units of the dataset, $\tau_G$/pc, to G-band extinction using the standard relation between optical depth and extinction:

$$A_G = 1.086 \tau_G.$$  \hspace{1cm} (6)

The line-of-sight resolution of the map is 1 pc. We obtain the cumulative extinction out to a certain distance along the line-of-sight by summing the optical depth per parsec over voxels out to that distance (and multiplying by the factor in equation 6).

To obtain an estimate of the total extinction along the line-of-sight, we use the map presented in Planck Collaboration Int. XXIX (2016)2 which was created by fitting the dust model of Draine & Li (2007) to dust emission and renormalized to match quasar extinctions.

2 The filename of the Planck total extinction map is: COM_CompMap_Dust_DL07-AvMaps_2048_R2.00.fits
This map is given in units of magnitudes in the V band, $A_V$.

We use the Fitzpatrick et al. (2019) extinction curve to convert the Planck $A_V$ to G-band extinction, $A_G$. The pre-launch Gaia G-band central wavelength is 0.673 μm (Jordi et al. 2010). We therefore take the inverse monochromatic G-band wavelength to be $1.5 \, \mu m^{-1}$, which corresponds to a value of $E(G - V)/E(B - V) = -0.63$ from table 3 of Fitzpatrick et al. (2019). We then use the equation 19 in their appendix B to obtain:

$$A_G = A_V \left( -\frac{0.63}{R_V} + 1 \right) = 0.796 A_V, \quad (7)$$

for the standard value of $R_V = 3.1$.

3. RESULTS

We begin in Section 3.1 by briefly discussing the comparison between the three tracers of the $B$-field on large scales. We then discuss our choice for studying two individual loops (I and IV) in more detail, whose results will be presented in the following sections.

3.1. Large-scale overview and choice of loops

Figure 2 presents the all-sky maps of the polarization angle of the synchrotron emission, dust emission, and stars as well as the angle differences between all three pairs of tracers at $N_{\text{side}} = 32$. Gray pixels denote areas that are masked from the analysis, as mentioned in Section 2.4, either because of low S/N ($S/N < 4$) or because they did not contain any stellar polarization measurement.

As shown in Fig. 2, there are large areas of sky with no data, even at this relatively low pixel resolution ($N_{\text{side}} = 32$ or $1.8^\circ$). The synchrotron map has the best coverage, while the dust emission and starlight maps are more limited. Nevertheless, even with limited coverage, it is clear from Fig. 2 that there is a large-scale coherency both in the Galactic plane and at high latitudes in all three tracers. As pointed out before (e.g., Wolleben et al. 2006; Sun et al. 2015; Planck Collaboration et al. 2015a), this points to a coherent and ordered magnetic field in general, which is also supported by observed high polarization fractions in the synchrotron emission (Vidal et al. 2015; Planck Collaboration et al. 2016a). More importantly, the angle difference maps (right-hand side of Fig. 2) show remarkable agreement between the three tracers of magnetic field orientation.

The overall alignment between these sets of tracers in the plane and at high latitude was already noted for polarization angles of starlight and dust emission (Planck Collaboration et al. 2015b, 2020b) while the correlation between synchrotron and dust emission was noted in Planck Collaboration et al. (2015a), particularly in the region around Loop I.

We note that the $\theta$ map includes only stars out to 1 kpc. The angle differences between stellar and synchrotron polarization ($|\theta - \phi_{\text{synch}}|$) indicate alignment for a substantial fraction of the high latitude sky. We find that 47% of the pixels at $|b| > 30^\circ$ have $|\theta - \phi_{\text{synch}}| < 20^\circ$ (our defined threshold for alignment, see Section 2.4). Such widespread alignment was also seen with fewer stellar measurements when comparing to WMAP data (Page et al. 2007). This alignment places an upper limit on the synchrotron emission: in these regions the high latitude polarized synchrotron emission must be dominated by the nearest 1 kpc. With wider and deeper coverage of stellar surveys we will be able to place more stringent limits on the fraction of emission that is contributed beyond this distance as a function of latitude.

The synchrotron and thermal dust angles are well aligned for most of the available sky, except for the inner plane ($|l| \lesssim 60^\circ$) at intermediate latitudes ($|b| \approx 5^\circ$–$20^\circ$), and a few other specific regions (e.g., near the Orion nebula). Areas of misalignment can also be informative. In these regions the synchrotron and dust emission are tracing different $B$-fields along the line-of-sight; either due to being at different distances, or a complex geometry producing different projections of the $B$-field on the sky.

For most of the high-latitude sky (76% of the unmasked pixels with $|b| > 30^\circ$), the $|\chi_{\text{dust}} - \phi_{\text{synch}}|$ map shows large, continuous regions with values $\lesssim 20^\circ$. Similar regions of alignment are found in the $|\theta - \chi_{\text{dust}}|$ map. This is not a surprise, since at high latitudes, the absorbing and emitting dust column is likely the same (as shown by Skalidis & Pelgrims 2019; Planck Collaboration et al. 2020b). At high latitudes, the large areas of alignment are particularly above the Galactic centre near Loop I. Notable areas of misalignment include Loops Is and XII where the angles can be discrepant by many tens of degrees. We note that in some of these pixels at high latitudes there is only a single star measurement, which may not be fully representative of the $B$-field along the line-of-sight depending on (a) the distance of the star and (b) whether the source is intrinsically polarized or not. However, in regions where multiple pixels show similar values, this is less of a concern.

At low latitudes, the regions with good agreement are likely due to the dominance of the $B$-field aligned with the spiral arms in the Galactic disk.

Our goal is to look for correlations between the various $B$-field tracers and, ultimately, place limits on the distance to the large-scale radio loops/spurs. We therefore
Figure 2. Maps of all three $B$-field angle tracers (left panels) and their pairwise absolute angle differences (right panels) in degrees. Synchrotron spurs are outlined in bright red (see also Fig. 1). Left panels: stellar polarization angle $\theta$ (top), synchrotron polarization angle, $\phi_{\text{synch}}$ (middle) and dust emission polarization angle, $\chi_{\text{dust}}$ (bottom). Angles are defined to follow the $B$-field orientation measured in Galactic coordinates from the Galactic North and increasing towards larger Galactic longitude, according to the IAU convention (see Section 2). Right panels: absolute angle difference between maps of $\theta$ and $\phi_{\text{synch}}$ (top), $\chi_{\text{dust}}$ and $\phi_{\text{synch}}$ (middle), and $\theta$ and $\chi_{\text{dust}}$ (bottom). All maps are in Mollweide projection, in Galactic coordinates, centered on $(l, b) = (0^\circ, 0^\circ)$. Grey pixels indicate no data or low S/N ($< 4$). Dotted grid lines are spaced by $30^\circ$. 
expect to be able to perform this correlation analysis for features that meet two conditions:

1. Stellar measurements towards the feature have a high enough density and area coverage.

2. Stellar polarization angles are in good agreement with synchrotron polarization angles, and hence can be assumed to be tracing the same $B$-field.

In practice, we are still very limited by the stellar polarization sampling. Only 2 out of the 14 features studied by Vidal et al. (2015) meet these qualitative criteria. Many loops only have a few stellar measurements that do not cover an appreciable fraction of their extent (IIIa, VIIb, X, XI, XIII, XIV) or have no measurements at all (XII).

Three loops do have good statistics of stellar measurements but the polarization angles of the stars are misaligned with respect to the synchrotron emission (III, VIII, GCS). This means that the locations of the dominant sources from each tracer, must be different, since they are tracking a different $B$-field direction. This misalignment could in principle be used to gain insight into the statistical variability of the $B$-field and properties such as field reversals (e.g., Jaffe 2019).

Loop I has tens of measurements within a single $N_{\text{side}} = 32$ pixel; these are targeted measurements towards the Corona Australis (CrA) molecular cloud (Heiles 2000; Targon et al. 2011), which has no specific relevance to this large-scale loop (see Bracco et al. 2020, for a detailed analysis of the magnetic field in this structure). Loop IX is in a region of small $\theta^* - \phi_{\text{synch}}$, however the coverage of stellar measurements is highly non-uniform, with very few stars coinciding with the ridge of synchrotron polarized intensity.

In the following subsections, we examine in detail the relation between starlight polarization and the synchrotron/thermal dust emission towards the two best-sampled radio spurs: Loop I and Loop IV.

### 3.2. Loop I

Loop I occupies the region of the high-latitude sky with the best sampling in terms of stellar polarimetry. As seen in Fig. 2, stellar polarization angles are well-aligned with synchrotron angles in this general area. In Fig. 3 we re-examine the correlation of stellar and synchrotron polarization angles towards Loop I in detail. The improvements include more stars, higher S/N radio polarization data, and, most importantly, reliable distance measurements from Gaia.

We select 4 circular regions ($I_A, I_B, I_C, I_D$) centered along the outline of Loop I that was defined in Vidal et al. (2015), to compare the polarization angles of stars and synchrotron emission as a function of stellar distance. The regions are outlined in Figures 1 and 3. Because of the strong depolarization of the synchrotron emission at low latitude ($b \lesssim 10^\circ$), where line-of-sight confusion is likely prominent, we focus this analysis on areas at higher latitude. For the selected regions we calculate the angle difference of each individual star with the synchrotron polarization angle of the $N_{\text{side}} = 32$ pixel it occupies. We choose a radius of $8^\circ$, wide enough to contain a large stellar sample, but small enough to avoid overlap with other features of the radio sky. The four regions are centered on the loop at increasing latitudes; their coordinates can be found in Table 1. In each region, we bin the stellar data in distance using a constant distance range of $50$ pc. The first bin edge is placed at the distance of the nearest star. In each bin we calculate the weighted mean angle difference using equation 1 and quantify the spread as the 16-84 percentile range. These values are shown along with the individual stellar measurements in Fig. 3 (upper sub-panels for each region). Bins with less than 2 stellar measurements are excluded from this calculation. Stars further than 1 kpc are not used, as they would not provide further constraining capability (the angle differences have already converged at much smaller distances, as seen in Fig. 3).

In all regions we find that the nearest distance bins spanning $[0, 100]$ pc, contain measurements with large uncertainties in $\theta^* - \phi_{\text{synch}}$. The uncertainties of the angle differences at these distances are dominated by the uncertainties of the stellar measurements, $\sigma_\theta^*$. The mean $\sigma_\theta^*$ is $\sim 20^\circ$ for regions $I_B, I_C, I_D$ in this range and $12^\circ$ for region $I_A$. The spread of the distribution of $\theta^*$ is also large. At larger distances, the stellar uncertainties decrease significantly (by about a factor of 3–5).

This behavior arises from the distribution of ISM dust within the vicinity of the Sun. We are located in a cavity of the ISM, known as the Local Bubble, where the dust volume density is low (Cox & Reynolds 1987). This cavity has recently been mapped with the use of stellar extinctions and distances (Lallemand et al. 2018; Pel-

### Table 1. Summary of location and distance measurements for the Loop I and IV regions.

| Region | Location ($l, b$) | Distance limits (pc) |
|--------|------------------|----------------------|
| $I_A$  | (32°10.19, 19°12) | –                    |
| $I_B$  | (33°95.38, 58°03) | 112 ± 17 pc          |
| $I_C$  | (26°68, 58°73)   | ≤ 105 pc             |
| $I_D$  | (358°17, 74°06)  | 135 ± 20 pc          |
| $IV_A$ | (328°74, 33°59)  | 180 ± 15 pc          |
| $IV_B$ | (302°72, 31°81)  | –                    |
Figure 3. Comparison between starlight and synchrotron polarization angles towards Loop I. The analysis is performed in four 16°-diameter circular regions (I_A, I_B, I_C, I_D). Left: Background: Polarized intensity of synchrotron emission at $N_{side} = 128$. Overlay: Stellar polarization segments for stars within 1 kpc (yellow) and synchrotron polarization segments (red) at $N_{side} = 32$. The stellar segment length is scaled by $1/\sigma^2_\theta$, while the synchrotron segment length is proportional to the polarized intensity. Pink circles mark regions I_A – I_D. The map is in Gnomonic projection. The polarization segment visualization is with respect to the direction of North of the center of the image. This does not affect the analysis. Right: (top sub-panel) $\theta^* - \phi_{\text{synch}}$ as a function of distance (light gray points). Angle differences are binned in distance and we show the mean angle difference in each bin (blue line) and the 16–84 percentile range (light blue shade). We do not show means for bins with less than 2 stars. Stars with distances $>1$ kpc are displayed at 950 pc for visualization but not included in the analysis. (Bottom sub-panel) Median cumulative G-band extinction as a function of distance, evaluated at the coordinates of each star in the circular region, from the 3D dust map of Leike et al. (2020) (red line). The pink range shows the 16- and 84 percentile of $A_G$. The total $A_G$ derived from Planck is shown as a solid brown line at large distances (median), with the orange band denoting the 68 per cent range. The angle difference map is at $N_{side} = 32$. 
To confirm that indeed the observed large uncertainties at small distances are due to a relative absence of dust, we employ the 3D dust extinction map of Leike et al. (2020).

We query the map to obtain the extinction profile at the coordinates of every star in our selected regions. Figure 3 (lower right sub-panels) shows the median, 16 and 84 percentiles of the distribution of $G$-band extinction towards the stars, $A_G$, as a function of distance. An abrupt rise in $A_G$ is seen at distances $\sim 100$ pc, in good agreement with the range of distances where we observe large $\sigma^*_\phi$. The rise in extinction coincides with a rise in the stellar polarization at these distances, as shown in Berdyugin et al. (2014) for the high-latitude parts of Loop I and in Santos et al. (2011) for the lower latitude area (our region $I_A$).

The mean values of $\theta^* - \phi_{\text{synch}}$ in the distance range $[100, 200]$ pc, are within $\pm 10^\circ$ for regions $I_B, I_C, I_D$. Within this distance range, the two tracers are probing the same orientation of the magnetic field. This remains the case at larger distances (out to 600 pc).

The lowest latitude region, $I_A$, shows a different behavior. While the mean angle differences are within $20^\circ$ of the origin for the distance range $[100, 200]$ pc, the standard deviation is large due to the substantial intrinsic scatter of the measurements. The mean angle between $\theta^*$ and $\phi_{\text{synch}}$ deviates gradually from zero at distances greater than $\approx 250$ pc, dropping from $\approx -5^\circ$ to $\approx -40^\circ$ at distances larger than 300 pc. The spread of the distribution of angle differences is large, and is dominated by astrophysical scatter; the uncertainties of individual $\theta^*$ are on average $< 5^\circ$. At these distances, stars in region $I_A$ are probing a magnetic field geometry that is different than that probed by the synchrotron emission. This is not unexpected since this region is the lowest latitude portion of Loop I studied here and therefore the line-of-sight magnetic field will be more complex. The dust and magnetic field responsible for polarizing stars further than 200 pc may be associated with the outskirts of the Aquila Rift, which extends over tens of square degrees to the right of the map and lies at a distance of 200–280 pc (Zucker et al. 2020).

So far, we have found an alignment between the mean stellar polarization angle and the magnetic field orientation traced by the synchrotron emission in the distance range $[100, 200]$ pc for $b > 30^\circ$. This is a strong indication that at high latitude, Loop I, which dominates the polarized synchrotron emission in the area, is located within this range of distances. This conclusion is in agreement with several other determinations of the distance to Loop I (e.g., Salter 1983; Vidal et al. 2015; Planck Collaboration et al. 2016a; Das et al. 2020).

In our analysis, we have calculated the angle difference between the synchrotron emission measured within 1.78 pixels, and individual stellar polarizations (measured within the arcsecond stellar PSF). The low spatial density of stellar measurements has necessitated this choice. However, it is natural to expect that this mismatch of spatial scales may contribute to the observed astrophysical scatter in the angle differences. If this is the case, we expect that the distribution of angle differences, if computed at the same resolution for both tracers, would show a tighter correlation than the distribution using individual stellar measurements. Though limited by the amount of stellar polarization data, we can gain further insight through the tight correlation between dust-induced polarization in absorption and in emission that holds at high Galactic latitude (Planck Collaboration et al. 2020b).

First, we search for the distance at which the correlation between dust emission and stellar polarization

![Figure 4. Difference between stellar and thermal dust B-field angles, $\theta^*$ and $\chi_{\text{dust}}$, in degrees, as a function of distance. The four panels represent the four regions selected for Loop I. Symbols are the same as in Fig. 3.](image)
angles occurs (as in Skalidis & Pelgrims 2019). Figure 4 shows the angle difference $\theta^* - \chi_{\text{dust}}$ as a function of distance for the four regions along Loop I. The two tracers are well-aligned for distances larger than 100 pc in regions I_B, I_C, and I_D. The statistics in region I_D are poor due to the low S/N of the Planck polarized dust emission data at high latitude, however all $\theta^*$ in the region lie within 1 $\sigma$ of $\chi_{\text{dust}}$. From the observed tight correlation we infer that the polarized dust emission is dominated by the dust at 100 pc in these regions.

While the polarized dust emission is mostly local in these high latitude regions, the cumulative extinction (Fig. 3) appears to rise out to the maximum distance of the 3D dust map (~400 pc). We can estimate the maximum amount of stellar polarization that this rise in extinction could produce, from the relation between reddening, $E(B-V)$, and maximum stellar polarization fraction, $p_{\text{max}}$: $p_{\text{max}} = 13\% E(B-V)$ (Panopoulou et al. 2019; Planck Collaboration et al. 2020b). For regions I_C and I_D, the rise from 150–400 pc would correspond to a change in fractional polarization of the stars of <0.06%, significantly less than the mean polarization of the stars in the region (0.15% and 0.3% for region I_D and I_C, respectively). In region I_B the rise from 150–400 pc is ~0.1 mag, which would correspond to a polarization of 0.3%, comparable to the mean polarization of stars in the region. The fact that we do not detect significant changes in the polarization angle suggests that the magnetic field geometry does not vary along the line-of-sight, even though the amount of dust (and polarization) may be increasing with distance.

We do note, however, that the observed rise in 3D extinction may be affected by systematic uncertainties. The median extinction from the 3D dust map does not reach the Planck value, which is probing the entire dust column. This discrepancy may be pointing to systematic offsets between the two datasets, which are constructed from entirely different tracers and methods. In fact, at high latitude, existing dust maps show significant systematic variations even among maps created using Planck data alone (see, e.g., Panopoulou et al. 2019). A detailed comparison between the 3D dust map of Leike et al. (2020) and the FIR-inferred extinction from Planck, though warranted, is beyond the scope of this paper.

The results in regions I_B, I_C, I_D are very different from those in region I_A. In this region the mean angle difference drops below 20° from 0° at ~200 pc, however a large spread remains (Fig. 4). This spread, along with the rise in $A_G$ in the region farther than 200 pc may indicate the presence of multiple dust structures with varying magnetic field geometries. At distances larger than 300 pc, the majority of stars have a $\theta^*$ within 16° of $\chi_{\text{dust}}$ and the median $A_G$ profile flattens. These in-
indications of the presence of material extended along the line-of-sight agree with similar conclusions from X-ray absorption studies at even lower latitude (Sofue 2015; Lallement et al. 2016).

Figure 5 shows the distribution of angle differences between all three pairs of B-field tracers towards Loop I: $|\theta^* - \phi_{\text{synch}}|$, $|\chi_{\text{dust}} - \phi_{\text{synch}}|$, $|\theta^* - \chi_{\text{dust}}|$. The distribution of angle differences takes into account all non-masked pixels within the circular regions defined in Fig. 3. As seen previously, stellar polarization in the higher latitude regions I_B, I_C and I_D is well aligned with $\phi_{\text{synch}}$. This is not the case in the lowest latitude region I_A, where we have established the contribution to the polarization of dust structures further than 200 pc (Fig. 4). In all regions, stellar polarizations are well-aligned with $\chi_{\text{dust}}$, as shown over most of the sky by Planck (Planck Collaboration et al. 2015b, 2020b), confirming that we can use dust emission to examine the effect that beam-averaged stellar polarizations would have. In regions I_B and I_C, we find the standard deviation of the distribution of $\theta - \phi_{\text{synch}}$ ($16^\circ \pm 1^\circ$ and $24^\circ \pm 3^\circ$) to be larger than that of the $\chi_{\text{dust}} - \phi_{\text{synch}}$ distribution ($9^\circ \pm 0.5^\circ$ and $9^\circ \pm 1^\circ$), as expected due to beam averaging. The standard deviation of the distribution of angle differences and its uncertainty were calculated from 1,000 Monte Carlo realizations, from which we report the mean and $1 - \sigma$ uncertainty. Region I_D (highest latitude region) has very few pixels with high enough S/N in the dust emission map.

The observed tight correlation between $\chi_{\text{dust}}$ and $\phi_{\text{synch}}$ in regions I_B and I_C lends additional support to the argument that the bright edge of Loop I lies at a distance of 100–200 pc. The dominant contribution to the synchrotron emission along the line-of-sight most likely arises from within the same volume that dominates the polarized dust emission (Fig. 4).

In conclusion, we present two pieces of evidence in support of the hypothesis that at $b > 30^\circ$, Loop I is a nearby structure (within 100–200 pc):

- The mean stellar polarization, averaged within regions I_B, I_C, I_D is aligned with the synchrotron magnetic field orientation within 100–200 pc.

- The dust emission polarization is well aligned with synchrotron in the regions where the total dust column is dominated by structures within a few hundred pc.

In the analysis so far we have presented a qualitative discussion of the behavior of the values of $\theta^* - \phi_{\text{synch}}$. We quantify the uncertainty in the distance determination in this paper compares to others in the literature in Section 4.

3.3. Loop IV

We next investigate the stellar polarization towards Loop IV (Fig. 6). We perform the analysis of angle differences in two circular regions of radius $8^\circ$, centered on the outline of Loop IV that was defined in Vidal et al. (2015). In both regions the binned angle difference $\theta^* - \phi_{\text{synch}}$ is significantly offset from zero for the majority of distance bins. The lowest (absolute) values of mean angle difference are found in region IV_A within 250–350 pc. We are faced with two apparently conflicting results: stellar and synchrotron polarizations are indicative of alignment in this distance range for region IV_A, but no such alignment is observed for its neighboring region IV_B. These results suggest two possibilities: (a) that Loop IV is located further than ~400–500 pc, where stars are lacking from our analysis, in which case the alignment in region IV_A at 250–350 pc is circumstantial, or, (b) synchrotron emission from regions IV_A and IV_B originates at drastically different distances.

We can test the first hypothesis by looking at the dust emission towards this structure. First, we examine the dependence of $\theta^* - \chi_{\text{dust}}$ in region IV_A (bottom left panel, Fig. 6). The angle differences $\theta^* - \chi_{\text{dust}}$ converge to zero for distances larger than 300 pc. The polarized dust emission is therefore dominated by dust within 300 pc in region IV_A. In region IV_B there are too few pixels with both stellar measurements and high S/N polarized dust emission at $N_{\text{side}} = 32$. We confirm that at $N_{\text{side}} = 16$, the mean difference $\theta^* - \chi_{\text{dust}}$ approaches zero at a distance of 300 pc, though the independent pixels with $\chi_{\text{dust}}$ measurements are only 10 (not shown in Fig. 6).

Next, we examine the distribution of absolute angle differences between pairs of all three magnetic field tracers (Fig. 7). For region IV_A, we find that the dust emission is tightly aligned with $\phi_{\text{synch}}$, more so than the stellar measurements. The standard deviation of the distribution of $\theta^* - \phi_{\text{synch}}$ is $25^\circ \pm 2^\circ$, versus $19^\circ \pm 1^\circ$ for the distribution of $\chi_{\text{dust}} - \phi_{\text{synch}}$ (where we report the mean and $1\sigma$ from Monte Carlo realizations taking into account the measurement uncertainties). We have established from our discussion of Fig. 6 that the polarized dust emission predominantly arises from within 300 pc. From their tight correlation, we conclude that the synchrotron polarization in region IV_A must be within 300 pc, co-located with the dust emission. However, the same situation does not hold for region IV_B. In this region, despite the fewer detections of $\chi_{\text{dust}}$, it is clear that the $\chi_{\text{dust}} - \phi_{\text{synch}}$ show a large spread, with no preferred
Figure 6. As in Fig. 3 but for Loop IV and for two regions (IV_A and IV_B). The lower left panel shows the difference between stellar polarization, $\theta^*$, and dust emission, $\chi_{\text{dust}}$, as a function of distance, as in Fig. 4 but for region IV_A.

Figure 7. Distributions of polarization angle differences between the three magnetic field tracers for each of the 2 regions centered on Loop IV (see Fig. 6).

alignment at 0°. A comparison of stellar polarizations with dust emission, suggests that in this region the polarized dust emission arises from within 300 pc (as in region IV_A). Since the dust emission is not aligned with $\phi_{\text{synch}}$ here, the synchrotron emission in region IV_B cannot be at the same distance as that in IV_A. It would have to be located further than the stars in our sample, i.e., further than 550 pc. Otherwise, it would need to have no dust associated with it. In both cases, we can deduce that IV_A and IV_B are not part of the same physical structure – the data favor hypothesis (b).

To the best of our knowledge, this is the first conclusion in the literature that Loop IV is not a coherent structure. The fact that $\phi_{\text{synch}}$ are misaligned with the
axis of the structure in region IV_A (as shown by Vidal et al. 2015) supports this conclusion. We note that Loop IV was first identified in total intensity (Large et al. 1966; Berkhuijsen et al. 1971) and was initially thought to be part of Loop I. Figure 8 shows maps of synchrotron total intensity at 408 MHz from Remazeilles et al. (2015) as well as the map of polarized intensity at 28.4 GHz from this work. We first note that the apparent loop in intensity, which is where it is most clear, is only visible on one side. Furthermore, the upper part is actually co-located with the ‘tip’ of Loop I where it fades into the background. Therefore, a large part of the circular feature may be due to chance alignment, especially given the morphology in polarization.

In polarized intensity the outline of Loop IV is not as continuous as in total intensity, with large gaps along it (see Fig. 8). The polarization angles do not trace the outline of the loop over most of its length (see also Vidal et al. 2015). Rather, the polarization angles appear as a continuation of the large-scale pattern that exists throughout a much larger area outside the loop (towards the left of the map). When comparing the polarization angle with the loop’s outline in the lower part of Loop IV, Vidal et al. (2015) find that the two are aligned only over the part of the structure that we define as region IV_B.

We speculate that the polarized intensity in region IV_B could be associated with a different structure than what has been traditionally defined as Loop IV. Upon inspection of the map in Fig. 6, we observe that the polarization pattern of the synchrotron emission in region IV_B appears as a smooth continuation of the upper part of Loop XIV (bright filament in the lower left corner of the map). Targeted observations of stellar polarization towards the region connecting these two structures would help test this hypothesis, and yield a distance limit to the associated structures.

As a final note, we mention the existence of the bright bubble in Hα discovered by Reynolds (1985) (shown in the bottom panel of Fig. 8), which appears co-located with the center of Loop IV. This H II region is associated with the bright binary star Spica (α Vir). The H II region is also observed in FUV spectral line emission (Park et al. 2010; Choi et al. 2013). With a Hipparcos parallax of 12.44 ± 0.86 mas (Perryman et al. 1997), the distance of Spica is 80 ± 5 pc. The H II region is therefore much nearer than where the synchrotron emission originates from in region IV_A, hence the two structures are most likely unrelated.

3.4. Calculating upper and lower distance limits for Loops I and IV

Having discussed the qualitative behavior of $\theta^*$ and $\phi_{\text{synch}}$ as a function of distance for the selected regions towards Loops I and IV (Sections 3.2 and 3.3), we proceed to place lower and upper limits on the distance to the synchrotron emission.

If $\theta^*$ and $\phi_{\text{synch}}$ are tracing the same magnetic field at a distance $D_{\text{synch}}$, we expect to observe mean angle differences $\theta^* - \phi_{\text{synch}}$ around zero for distances further than $D_{\text{synch}}$. This places an upper limit on the distance
of the synchrotron emission. In practice, we search for
distance bins where two criteria for alignment are met:

1. The absolute value of the circular mean of \( \theta^* - \phi_{\text{synch}} \) in a bin is \( \leq 20^\circ \) and

2. The PRS within the bin is higher than the 99.9 percentile of the distribution of PRS drawn from
a uniform distribution (equivalent to a significance threshold of 3\( \sigma \)).

As the various sources of noise (measurement uncertainty, intrinsic astrophysical scatter) can cause spurious
cases in which these criteria are met, we search for dis-
tance ranges where the conditions are met over multiple
bins.

Placing a lower limit on the distance is less straight-
forward, especially if there is significant contribution from
-Field foreground to \( D_{\text{synch}} \). Fortunately, we
have established that for regions I\(_B\), I\(_C\), I\(_D\), there is little
foreground contamination up to the distance where we
observe alignment (dust extinction is low at distances
\(< 100 \text{ pc} \)). Region IV\(_A\) also exhibits alignment after
some distance, even though the dust extinction continues
to rise up to 400 pc, suggesting that the foreground
dust is not dominating the polarization signal. To place
a lower limit on the distance to the synchrotron fea-
tures, we can use the fact that the mean \( \theta^* - \phi_{\text{synch}} \) will
in general be non-zero at distances where the stars are
tracing a different magnetic field than the synchrotron.

We search for bins where the mean \( \theta^* - \phi_{\text{synch}} \) shifts
from significantly non-zero values to being consistent
with zero. Specifically, distance bin \( i \) will fit the cri-
tera for a lower distance limit if:

\[
\mu^{i+1} \leq 20^\circ \quad \text{and} \quad \mu^{i+1} - \mu^i \geq 2\sigma_{\mu^i},
\]

where \( \mu^i \) is the mean value of the \( \theta^* - \phi_{\text{synch}} \) in distance
bin \( i \), and \( \sigma_{\mu^i} \) is the uncertainty on \( \mu^i \), calculated as the
standard deviation from 10,000 random realizations of
the data in the bin (the same realizations used to obtain
uncertainties in the PRS, discussed below). Obviously,
the center of bin \( i \) must be at a smaller distance than the
upper limit on the distance, as defined by the criteria (1)
and (2) mentioned previously.

Before we proceed, we must take into account the fol-
lowing sources of uncertainty that were ignored in the
analysis of Sections 3.2 and 3.3: (a) the selection of
distance bins, and (b) the statistical significance of the
alignment, as quantified by the PRS.

**Placement of distance bins.** To quantify whether stel-
lar and synchrotron polarization angles are statistically
aligned at a certain distance, we bin the \( \theta^* - \phi_{\text{synch}} \)
measurements in distance steps of 50 pc. In Sections 3.2
and 3.3 we showed one such choice of bins. We inves-
tigate the effect of shifting the bin locations on the ob-
served correlations as follows. Starting from a distance
of 0 pc, we define bins of size 50 pc out to a distance of
1 kpc. Thus, the first bin spans [0, 50] pc, the second [50, 100] pc etc. We compute the circular mean and PRS in
each bin that contains more than 2 stars. We repeat this
process by shifting the bins by 10, 20, 30 and 40 pc. The
measured circular mean and PRS in all bins are shown in
Fig. 9.

**Measurement uncertainties and the significance of the
PRS.** We explore the effect of uncertainties of individ-
ual measurements as follows. We ‘re-observe’ each angle
difference measurement by drawing from a normal dis-
tribution with mean equal to the observed angle difference
\( \theta^* - \phi_{\text{synch}} \) and standard deviation equal to the meas-
urement uncertainty. We repeat this process 10,000 times
for each bin. We recompute the mean angle difference
and PRS for each iteration. The standard deviation of
the values is the error on the mean angle difference and
PRS in each bin.

To quantify the statistical significance of the align-
ment, we compute the PRS for random realizations of
measurements drawn from a uniform distribution (Jow
et al. 2018). Each mock angle difference is drawn from
a normal distribution with mean a random value in the
range \([-90^\circ, 90^\circ]\) and standard deviation equal to the meas-
urement uncertainty. If the observed PRS value is
larger than the 99.9 percentile of mock (uniform) PRS
values in that bin, then the alignment is statistically
significant (at a level of \( \geq 3 \sigma \)).

**Distance determination.** The results in Fig. 9 con-
firm the qualitative result that alignment of \( \theta^* - \phi_{\text{synch}} \)
is found for regions I\(_B\), I\(_C\), I\(_D\), IV\(_A\) and not for regions
I\(_A\), IV\(_B\). Region I\(_A\) shows an example of spurious align-
ment in Fig. 9 for the bin centered on 85 pc. Neighboring
bins do not meet both alignment criteria.

Region I\(_B\) shows alignment for distance bins over a
wide range: the alignment conditions are met for the
bins centered at 130 pc out to 385 pc. Thus, the upper
limit to the distance of the synchrotron emission in the
region is 130 pc. The lower distance limit criterion is
met for the bin centered on 95 pc. We thus conclude
that the synchrotron emission from region I\(_B\) must arise
within the range [95, 130] pc. Since the bin spacing is
10 pc, these values may vary within \( \pm 10 \text{ pc} \).

We follow the same process to place distance limits for
region I\(_C\). The distance bin centered on 105 pc is the first to meet the alignment criteria. The alignment
criteria are met for bins spanning [105, 335] pc. At small
distances, the PRS is within 3\( \sigma \) of the uniform case, indi-
cating that the observed small values of the mean angle
difference are not statistically significant. The fact that we do not observe a shift in the mean values with distance precludes the determination of a lower distance limit. We do note that the low PRS values coincide with a distance range devoid of dust (see Section 3.2). This distribution of dust with distance would suggest that the dust causing the polarization of stars is beyond 55 pc. The synchrotron emission in region I_C likely exists within the range [55, 105] pc. However, the stellar polarization data alone only allow us to place confidence in the upper limit of 105 pc.

In region I_D the alignment criteria are met in the narrow range of distances for bins centered at [155, 235] pc. The values of the PRS are lower compared to other regions, due to the increased uncertainty in the stellar polarization measurements. We can place a conservative upper limit on the distance to the synchrotron emission in region I_D of ≤ 155 pc. The lower limit is found at 115 pc. Thus, the distance to the synchrotron emission in region I_D is [115, 155] pc. A larger number of more precise measurements would be needed to give tighter constraints.

We have attempted to combine the stellar measurements in all three regions of Loop I with distance constraints, in order to increase the statistics of the number of stars and obtain a more precise measurement of the distance. However, combining these measurements results in much increased scatter per distance bin. This increased scatter may be related to the fact that there seems to be a distance gradient with latitude, as shown by the stellar extinction measurements of Das et al. (2020). These authors find that the distance to the dust layer associated with Loop I varies gradually with latitude from 131 ±7 pc (at $b = 32^\circ$) to 70 ± 4 pc (at $b = 55^\circ$).

Region IV_B shows no bin with alignment. The PRS is low throughout the observed distance range, suggesting that along the sightline there is no dust feature that is co-located with the synchrotron emission and would cause the polarization of stars to trace the same $B$-field as the $\phi_{\text{synch}}$ (see Section 3.3).
Finally, region IV$_A$ shows alignment for the bins centered on [195, 365] pc. As discussed further in Section 3.3, the alignment between stellar polarization and polarized dust emission also occurs at comparable distances. We can thus place an upper limit on the location of the synchrotron emission at $\leq$195 pc. The condition for the lower distance limit is found at 165 pc. Our estimate of the location of the region’s synchrotron emission is [165, 195] pc.

The distance limits for all regions are summarized in Table 1. For ease of use we report the middle of each limiting distance range as the distance to the feature with uncertainties spanning the full range of the distance bracket.

4. DISCUSSION

We have compared the polarization angles of synchrotron and dust emission with measurements of starlight polarization as a function of distance to obtain limits on the location of two synchrotron features: Loop I and Loop IV, as defined by Vidal et al. (2015). We now discuss our findings for the distance to these structures in the context of the literature for each loop.

4.1. Loop I

The distance to Loop I and its brightest part (the NPS) has been the subject of numerous studies (for recent literature reviews see Planck Collaboration et al. 2016a; Dickinson 2018; Kataoka et al. 2018; Shchekinov 2018).

The high Galactic latitude part of Loop I ($b > 40^\circ$) was first measured to be at a distance of 100 $\pm$ 20 pc, on the basis of comparing the optical polarization of $\sim$10 stars with synchrotron polarization (Bingham 1967). Subsequently, Spoelstra (1972) confirmed that the observed correspondence between optical and radio polarization holds for stars in the distance range 50–100 pc. Ellis & Axon (1978) noted the correspondence remains for stars in the range 50–300 pc. As more optical measurements became available, the correlation has been noted in multiple subsequent works (e.g., Leroy 1999; Santos et al. 2011; Berdyugin et al. 2014). Our results for regions I$_B$, I$_C$, and I$_D$, are in excellent agreement with these previous determinations. We do note, however, that the aforementioned literature estimates were based on the comparison of individual stars with synchrotron polarization angles and as such did not budget for uncertainties due to beam effects or intrinsic scatter of stellar measurements within the selected sky regions. We have shown in Sections 3.2 and 3.4 that both factors come into play when considering the angle differences $\theta^* - \phi_{\text{synch}}$. The distance limits that we have placed are conservative and account for these uncertainties. More precise determinations would require a better sampling of stellar measurements both in distance and on the plane of the sky.

Through morphological comparison, the NPS has been associated with a region of bright X-ray emission extending from the Galactic plane to high Galactic latitude (e.g., Borken & Iwan 1977; Egger & Aschenbach 1995; Snowden et al. 1995). Other determinations of the distance to Loop I rely on morphological correlation of either the radio Loop I and/or the X-ray NPS with different tracers, including H I line emission (e.g., Berkhuijsen et al. 1971), stellar extinction (e.g., Reis & Corradi 2008), as well as dust emission and FUV lines (e.g., see maps in Park et al. 2007). H I structures in the vicinity of the NPS at latitudes $b > 55^\circ$ are located at 95–157 pc, shown by interstellar absorption lines in stellar spectra (Puspitarini & Lallement 2012). Stellar extinction towards the high latitude dust neighboring the NPS ($b = 26^\circ$–55$^\circ$) arises in the range 70–135 pc (Das et al. 2020). These determinations are extremely precise (e.g., Das et al. 2020, give systematic uncertainties of 4–7 pc towards individual regions). Using existing stellar polarization data alone, the distance determination is an order of magnitude less precise. Despite this shortcoming, there is a significant added benefit in using stellar polarization, as we argue next.

At high latitude, the stellar polarization data tie together the dust-bearing, cold medium that forms H I arches and causes the extinction and polarization to nearby stars (Iwan 1980; Puspitarini & Lallement 2012; Das et al. 2020) with the radio Loop I through the excellent observed correlation between the stellar and radio polarization angles. A coincidence between the spatial distribution of the cold gas with the radio emission is much harder to argue for (e.g., as done in Lallement et al. 2018) if one takes into account this long-standing observational fact. The alignment between stellar and synchrotron polarization angles starting at $\sim$100 pc (Figs. 3, 9) in regions I$_B$ and I$_C$ ($60^\circ > b > 30^\circ$) leaves little room for contribution of background emission to the polarization at 30 GHz. At the highest latitude range studied (region I$_D$) more stellar polarization data are needed to reduce observational uncertainties and confirm whether this conclusion is valid there as well.

From the above reasoning, radio synchrotron polarization, H I emission, dust emission/stellar absorption and optical polarization data are definitely linked. For the X-ray data, however, the link is less strong. Whether the X-ray NPS at high latitude is physically connected to the radio Loop I and (therefore to the above tracers) can be
argued mainly on the basis of morphological similarity (e.g., Iwan 1980, and references therein). Another potential means for connecting X-rays with cold gas/dust tracers is the column density inferred by modeling the X-ray spectrum, which has been used to place tight constraints for the distance to the structure at low latitudes ($b < 9^\circ$, Lallement et al. 2016; Das et al. 2020). Akita et al. (2018) modeled Suzaku data of the NPS at high latitude, finding that the necessary X-ray absorbing column is consistent with the total column density along the line of sight. Their finding is not particularly constraining, as the total column is contained within 75 pc at these latitudes, as shown using stellar extinction data by Das et al. (2020). Consequently, morphological similarity is the only argument that remains to suggest that the high-latitude X-ray NPS and the radio Loop I are parts of the same structure – a point we will return to shortly.

The finding that at high latitude the polarized radio Loop I is at $\sim 100$ pc is in apparent contrast with the conclusions drawn from recent studies that analysed X-ray data (Akita et al. 2018; LaRocca et al. 2020) and Faraday rotation (Sun et al. 2015; Xu & Han 2019). There are three arguments put forward to argue that the NPS is further than 200 pc.

The first argument, put forward by Xu & Han (2019), relies on the dispersion measure of the pulsar PSR J1503+2111 ($l, b = (29^\circ, 1, 59^\circ, 3)$). These authors derive a mean electron density towards the pulsar of 0.013 cm$^{-3}$, by assuming a uniform ISM density. This value is then compared to a model for the electron density of Loop I presented in Yao et al. (2017). Because the inferred electron density towards the pulsar is found to be two orders of magnitude less than the model, the authors conclude that Loop I must be background to the pulsar. However, the ISM density is not uniform along the 240 pc sightline towards the high-latitude parts of Loop I. In fact, the dust distribution shows an abrupt rise at about 100 pc, from both starlight polarization and extinction (Fig. 3 and also Das et al. 2020). We recalculate the electron density here. We know that almost 100% of the dust column is within $\sim 70$ pc (highest latitude region in table 2 of Das et al. 2020), most of it localized in a thin shell$^3$. Taking the thickness to be 1–10 pc, from the DM we would infer an electron volume density of 0.3–3 cm$^{-3}$, which is at most a factor of 3 different to the Yao et al. (2017) model (1.9 cm$^{-3}$). In addition to this, the comparison to the Yao et al. (2017) model may be erroneous, since the data show negligible dispersion measure at high latitude, with most pulsars constraining the model being at latitude $b < 20^\circ$. We conclude that the observed DM towards this pulsar is not in tension with the stellar polarization determination of the distance to the high-latitude parts of Loop I.

The second argument, presented in Akita et al. (2018), uses X-ray spectral information. The authors assume a uniform density throughout the line-of-sight and a plausible volume density of electrons for the X-ray emitting gas in the NPS. One can then divide the measured emission measure from X-ray data by the square of the assumed volume density to infer the line-of-sight path length. This leads to an estimate of 1–8 kpc, depending on the assumed volume density, which the authors use to argue in favor of a Galactic center distance to the NPS. However, for the same reasons discussed above, a uniform density assumption for the medium towards the NPS is unjustified. The fact that the emission measure depends on the square of the electron volume density, means that any clumpiness (i.e., volume filling factor less than unity) would accentuate the problem. Such assumptions can lead to erroneous conclusions, in contrast to the high-confidence measurements from stellar data.

The third argument was made by Sun et al. (2015), based on Faraday rotation of the diffuse synchrotron emission. These authors find that the Faraday depth towards the NPS at high latitude is consistent with zero, with all of the observed Faraday depth being attributed to the medium in the background of the NPS. Since the $B$-field is expected to lie parallel to the Galactic plane, they conclude that the $B$-field at high latitude will have only a small line-of-sight component, causing the Faraday depth to rise slowly as a function of distance. Thus, they expect the NPS at $b > 50^\circ$ to be several hundred parsecs away. The behavior of the Faraday depth at lower latitude is very different, which leads them to propose that the emission from lower latitudes arises from a longer path length.

As a final note, we mention one more argument that has been presented against the local SNR model for Loop I. Sofue (2000) argue that if the structure is local, it would be the only one of its kind because its physical diameter of $\sim 200$ pc would be much larger than that of typical SNRs. We note that structures of similar size exist in the local ISM: a prominent example is the Orion-Eridanus superbubble, at a distance of 400 pc. It has a diameter of 200 pc and was created by the combination of energy output from multiple young stars and possibly supernova explosions (see Soler et al. 2018, and refer-

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$^3$ This agrees with the 3D dust map of Leike et al. (2020) for all regions except I$_D$, for which we see a gradual rise in extinction in Fig. 3. The extinction values in this region are very low and could be prior-dominated.
ences therein). Similar activity from the Sco-Cen association could easily have created this very large nearby bubble that is the North Polar Spur (e.g., as suggested by Egger & Aschenbach 1995), meaning that Loop I may only be one of many reheated SNRs.

From the above discussion, we conclude that there remains no contradiction between the measurements of the distance to Loop I at high latitude and the evidence presented in the literature – the contradiction is in the conclusions that have been drawn. At lower latitude ($b \lesssim 10^\circ$), the situation is even more complicated, with many works using X-ray data (Akita et al. 2018; Kataoka et al. 2021; Predehl et al. 2020) and concluding that the NPS is located near the Galactic center, in support of the model proposed by Sofue (1977, 2000). These works assume that Loop I (and similarly the NPS which is associated with it) arise from a single structure. However, as argued by Dickinson (2018), if this assumption is lifted, then the superposition of multiple structures can explain the low latitude parts of Loop I, without the need to ignore/refute the very accurate nearby distance of the high latitude portion. Indeed, evidence has accumulated that this line-of-sight confusion is prevalent at low latitudes.

Several lines of evidence point to a superposition of multiple structures along the line of sight that gives rise to the radio and X-ray emission at intermediate to low latitude. For example, at latitudes $b < 9^\circ$, Lallement et al. (2016) find that the X-ray data require an absorbing column that places the emission further than 800 pc. Indeed, Lallement et al. (2018); Das et al. (2020) show the existence of multiple dust structures along the line-of-sight towards these low latitude regions. Sofue et al. (2016) compare the morphology of X-ray data with the radio continuum and conclude that the X-rays are absorbed by the Aquila Rift clouds (below $b < 30^\circ$), and therefore must be beyond 1 kpc. Our results for region $I_A$, at latitude $10^\circ$–$25^\circ$ show the lack of alignment between stars and synchrotron polarization angles, and are consistent with these conclusions.

While we are not able to disentangle the effect of the NPS at low latitude from background contributions, better sampled data might be able to do so. For example, Jones et al. (2016) show that NIR stellar polarization is perpendicular to the Galactic Plane at the base of the NPS ($b \sim 0.2^\circ$) at distances of a couple hundred parsecs.

In Fig. 10 we examine the morphology of the polarized radio intensity and X-ray data from ROSAT (band B6 at 0.73–1.56 keV). The well-known offset between radio Loop I and the X-ray NPS (e.g., Kataoka et al. 2021) is best seen by comparing the relative location of the emission to the line that traces the peak intensity of the polarized emission of Loop I from Vidal et al. (2015). This line neatly bounds the bright NPS as seen in the X-ray map. This remarkable morphological similarity, strongly suggests that the X-rays and radio are part of the same object, as previously noted in various works (e.g., Borken & Iwan 1977). This would mean that our distance constraints on the Loop I polarized radio emission apply to the X-ray NPS as well (for the regions studied, namely $b > 30^\circ$).

We propose the following hypothesis for explaining the combination of radio, optical and X-ray data, where the apparent contradiction between distance estimates is more prominent in the recent literature. At high latitude, the bulk of the radio polarization, the extinction, and stellar polarization are all local (within $\approx 100$ pc), as necessitated by the measurements of Puspitarini & Lallement (2012); Das et al. (2020) and this work. However, not all of the high-latitude X-rays attributed to the NPS need be local. The recent e-ROSITA finding of a symmetric, but much fainter X-ray lobe in the South (Predehl et al. 2020) leads us to the hypothesis that there is an equally faint Northern Galactic center lobe, on top of which there is superimposed local X-ray emission. As argued by several authors (e.g., Borken & Iwan 1977; Iwan 1980), the radio and X-ray emission requires a reheating episode of an old SNR by a more recent event. The asymmetric appearance of the radio Loop I is easily explained by the local reheated SNR hypothesis (e.g., Heiles et al. 1980; Wolleben 2007). If the entire X-ray emission were due to activity in the Galactic center\footnote{The X-ray e-ROSITA emission has been suggested to be associated with the Fermi Bubbles (Predehl et al. 2020).}, the observed asymmetry between the two hemispheres would require a corresponding asymmetry in the Galactic halo (the argument proposed by Sarkar 2019). In our view, the local SNR hypothesis for the high-latitude part of the NPS is not only a more plausible explanation, it is the only explanation that is consistent with the wealth of observational constraints on the distance to the structure, as discussed above.

4.2. Loop IV

In contrast to Loop I, the distance to Loop IV has received much less attention. Ellis & Axon (1978) searched for a signature of Loop IV in the polarization of stars but were unsuccessful due to lack of stellar measurements. With improved statistics we are able to revisit the relation between the radio emission and starlight polarization in parts of Loop IV. Our analysis has relied critically on the comparison between all three tracers of the
We find evidence that Loop IV is likely a superposition of discrete structures along the line-of-sight. To the best of our knowledge, this is the first evidence to date against the common assumption of Loop IV being a spherical shell, visible as a small circle in the sky. In hindsight, another indication of this can be traced back to Heiles & Jenkins (1976), who examined the morphology of HI gas towards Loop IV. They found some HI structures that morphologically resembled parts of Loop IV, but there were no features that matched the radio continuum morphology over the entire circumference of Loop IV.

Spoelstra (1973) estimated a distance to radio Loop IV by fitting a spherical SNR model (van der Laan 1962) to the total intensity at 1.4 GHz. He found a value of 250 pc for the distance to the center of the sphere. Given the observed radius in the sky of 20°, this would place the southern tangential endcap of the sphere (our regions IV_A and IV_B) at a distance of 235 pc. This is not consistent with our distance limits on region IV_A of [165, 195] pc. The results of Spoelstra (1973) rely on the model assumptions of a spherical shell expanding in a homogeneous medium. As discussed in Section 3.3, our multi-tracer comparison of polarization angles strongly suggests that Loop IV is not a single spherical structure.

Based on the Loop IV distance estimate of Spoelstra (1973), Borken & Iwan (1977) and Iwan (1980) suggested that Loop IV could be a young SNR that is interacting with Loop I (assumed to be a Myr-old SNR) and re-heating it. Our distance limits on Loop IV would place part of it (region IV_A) at a larger distance of [165, 195] pc compared to the distance of [95, 130] pc (our tightest limit on the distance to Loop I). With increased stellar polarization measurements we will be able to improve upon these constraints. We note that a recent analysis of γ rays also indicates a nearby distance to both Loop I and IV (Jóhannesson & Porter 2021).

5. CONCLUSIONS

We have combined optical stellar polarization with polarized dust and synchrotron emission to investigate the correlation of these magnetic field tracers towards high-latitude synchrotron spurs. Our findings are listed below:

- There is an overall tight correlation between the polarization angles of synchrotron, dust emission and stars at high galactic latitude, confirming earlier comparisons.
- In regions where the tracers $\theta^*$, $\phi_{\text{synch}}$ and $\chi_{\text{dust}}$ are well-aligned, we have used their correlation as function of stellar distance to place distance limits on Loop I and Loop IV.
- For Loop I we find that $\theta^*$ and $\phi_{\text{synch}}$ become well aligned at a distance of $\sim 100$ pc, confirming earlier evidence that the high-latitude portion of this structure is nearby. At the lowest latitude portion of the Loop studied here ($b \sim 20^\circ$) $\theta^*$ and magnetic field: starlight, synchrotron and dust emission polarization angles.

Figure 10. Comparison between radio and X-ray data. Left: Composite image with synchrotron polarized intensity (this work, yellow), and X-rays from ROSAT’s R6 0.73–1.56 keV band (Snowden et al. 1997) (blue). Middle: X-ray map of the ROSAT R6 band (units of $10^{-6}$ counts/s/arcmin$^2$) with the outline of radio Loop I from Vidal et al. (2015) marked with a red line. Right: Polarized intensity of synchrotron emission (this work) with the outline of Loop I as in the middle panel (units of mK). All images have a linear colorscale, $N_{\text{side}} = 128$, and are in Orthographic projection centered at $(l, b) = (30^\circ, 30^\circ)$. Grid lines are spaced by 30°. Lines of constant galactic longitude, $l = 0^\circ$ and constant latitude, $b = 0^\circ$, are marked solid white.
\(\phi_{\text{synch}}\) are not statistically aligned and their relative orientation varies with distance, suggesting the presence of overlapping features along the line of sight (Sections 3.2 and 3.4).

- For Loop IV we find a tight correlation between \(\chi_{\text{dust}}\) and \(\phi_{\text{synch}}\) for only part of the structure, for which we place distance limits. The observed lack of correlation towards a significant part of the loop suggests that radio Loop IV results from a superposition of unrelated structures along the line of sight (Sections 3.3 and 3.4).

- We propose a hypothesis that can reconcile the apparent inconsistency between the distance to the NPS from X-ray data and other distance constraints (Section 4).

The main limitation in our analysis is the lack of starlight polarization coverage. Further progress on placing distance limits to the majority of synchrotron loops will require an order of magnitude increase of stellar measurements in these regions, in order to obtain adequate statistics with distance. New data are anticipated over the next few years, which will open up large-scale multi-tracer studies of the Galactic magnetic field and structure. Dedicated optical starlight polarization surveys will improve the depth, accuracy, and most importantly, the sky coverage. The PASIPHA\'E survey (e.g., Tassis et al. 2018) aims to measure the polarization of millions of stars towards high Galactic latitude, producing more than 100 stellar measurements per square degree. Higher signal-to-noise ratio all-sky synchrotron polarization maps will also soon be available at 5 GHz from the C-Band All-Sky Survey (C-BASS; Jones et al. 2018), which will provide almost full-sky coverage with high S/N and minimal contamination from Faraday Rotation. Combining these maps with existing data from Planck, WMAP, the S-band Polarization All Sky Survey (at 2.3 GHz, Carretti et al. 2019) and the Q-U-I Joint Tenerife Experiment (at 10–42 GHz, Rubio-Mart\'in et al. 2012) will allow for much more precise determinations of synchrotron polarization angles at high latitude. At even lower frequencies (\(\sim 100\) MHz), data from the Low Frequency Array (LOFAR) will enable a tomographic view of the synchrotron emission, opening up new avenues to disentangle the contribution from multiple emitting components along the line of sight (Van Eck et al. 2019).

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Facilities: WMAP, Planck, Gaia

Software: astropy (Astropy Collaboration et al. 2018), HEALPix (G\'orski et al. 2005), healpy (Zonca et al. 2019)
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