Large-Scale Domain Engineering in Two-Dimensional Ferroelectric CuInP$_2$S$_6$ via Giant Flexoelectric Effect

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**ABSTRACT:** Room-temperature ferroelectricity in two-dimensional (2D) materials is a potential for developing atomic-scale functional devices. However, as a key step for the technology implementations of 2D ferroelectrics in electronics, the controllable generation of uniform domains remains challenging at the current stage because domain engineering through an external electric field at the 2D limit inevitably leads to large leakage currents and material breakdown. Here, we demonstrate a voltage-free method, the flexoelectric effect, to artificially generate large-scale stripe domains in 2D ferroelectric CuInP$_2$S$_6$ with single domain lateral size at the scale of several hundred microns. With giant strain gradients ($\sim 10^6$ m$^{-1}$), we mechanically switch the out-of-plane polarization in ultrathin CuInP$_2$S$_6$. The flexoelectric control of polarization is understood with a distorted Landau–Ginzburg–Devonshire double well model. Through substrate strain engineering, the stripe domain density is controllable. Our results highlight the potential of developing van der Waals ferroelectrics-based flexible electronics.

**KEYWORDS:** 2D ferroelectrics, CuInP$_2$S$_6$, flexoelectricity, polarization, artificial domains

Atomically thin van der Waals (vdW) crystals provide the opportunity to explore ferroelectricity at the two-dimensional (2D) limit which is a long-sought goal in conventional bulk ferroelectrics due to the constrain of critical size effect.† Experimentally, a series of 2D ferroelectrics with intrinsic either in-plane or out-of-plane electric polarization have been verified, such as the SnTe family,2−4 NbO$_3$ family,5 CuInP$_2$S$_6$,6−11 α-In$_2$Se$_3$,12−17 Br$_2$O$_3$Se$_2$,18,59 and d1T-MoTe$_2$.20 Along with the atomic thickness, vdW material also offers the layer degree of freedom that leads to the emergence of sliding ferroelectricity induced by interlayer translation.21−23 The rich 2D ferroelectricity found in vdW crystals therefore provides the potential to revolutionize future electronic applications with exotic functions.24−27

For the integration of 2D ferroelectrics in electronics, how to effectively control the polarization state or ferroelectric domains is the central concern because it fundamentally determines the technical practicability. In bulk ferroelectrics, it can be simply realized by applying an external voltage.28,29 For example, reliable domain structure in ferroelectric oxide thin film can be artificially created with the aid of a conductive tip in a scanning probe microscope (SPM).30−32 Nevertheless, for vdW ferroelectrics with atomic thickness the out-of-plane switching electric field at the 2D limit inevitably results in large leakage current and even material breakdown. As a result, the polarization control and especially the large-scale domain generation is relatively challenging in 2D ferroelectrics. Therefore, an alternative method which is free of external voltage is highly in demand for domain manipulation in vdW ferroelectrics.

Here, to address the above issue we utilize the flexoelectric effect, a voltage-free mechanical method, to switch the electric polarization and generate artificial domains at large-scale in ultrathin vdW ferroelectrics. The flexoelectric effect (or flexoelectricity) refers to the formation of net electric polarization inside a crystal when an inhomogeneous strain is applied.33−34 This effect is universal for all materials with arbitrary lattice symmetry and thus has been utilized to generate many extraordinary phenomena and functionalities such as enhanced piezoelectricity,35−38 the nanoscale polar vortices,39 and anomalous photovoltaics.40−42 To utilize flexoelectricity in polarization reorientation, the key is the generation of giant strain gradients.43,44 In conventional oxides ferroelectrics, due to the bulk nature with rigid covalence/ionic bond, mechanical domain control is generally realized under the involvement of an SPM tip via nanoscale imprinting or through atomic-scale misfit lattice strain.45−49 For 2D vdW ferroelectrics with genuine mechanical flexibility, the flexo-

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metal cations with In\textsuperscript{3+} sitting near the center and Cu\textsuperscript{+} supporting this framework; the other two-thirds are one-third of these cages are taken by the P\textsuperscript{−}\textsuperscript{2+} dimers. The sulfur atoms in the anion sublattice form octahedral cages.

Ionic bonds associated with the Cu\textsuperscript{+} and In\textsuperscript{3+} cation sublattices.

When reversing the polarization, the degeneracy of the ground states should be lifted off via external stimulus such as electric field or inhomogeneous strain (i.e., strain gradients) that lowers the switching energy barrier between the two energy minima. The latter, known as the flexoelectric effect,\textsuperscript{33,34} is with the benefit of voltage-free and large-scale uniformity for 2D vdW ferroelectrics which have atomic scale thickness and ultrahigh flexibility. Therefore, we apply this method to ultrathin CIPS in this study.

CIPS thin flakes were mechanically exfoliated from the bulk and were transferred onto the Au/SiO\textsubscript{2} substrate (detailed in Supporting Information). The single crystal nature of the samples studied here was confirmed by Raman spectroscopy (see Figure S1), where featured phonon modes were observed. The room-temperature ferroelectricity in CIPS can be evidenced from two aspects. As shown in Figure 1b, typical single/butterfly like ferroelectric hysteresis loop in the PFM phase/amplitude spectra were measured from a 20 nm thick CIPS sample. We estimate the coercive field for ultrathin CIPS to be around 3.5 × 10\textsuperscript{5} V/cm. This value is consistent with the results in previous studies.\textsuperscript{7} Furthermore, spontaneous domains with unambiguous domain wall structures are clearly visualized in Figure 1c (PFM phase image) and Figure S2b (PFM amplitude image). By carefully examining the domain size, we find that the domains in ultrathin CIPS are fractional with typical size of around 0.2 µm\textsuperscript{2} (see Figure S2c). The scattered domains are due to the ferroelectric transition temperature (T\textsubscript{c}) of CIPS at ~315 K, which is close to room temperature. Therefore, under ambient conditions strong thermal fluctuation will hinder the formation of large size domains in CIPS. Besides, we also carried out PFM tests on an 18 nm thick CIPS thin flake with 0.5, 1, and 2 V\textsubscript{AC} respectively, to exclude the influence of the AC voltage on the ferroelectric domain structures (see Figure S3). We also used the DC electric poling via PFM to check the quality of artificial domains. As shown in Figure S4, a box-in-box pattern has been poling with ±7 V\textsubscript{DC} tip bias. However, consistent with other

**Figure 1.** Methods of polarization switching in 2D ferroelectrics. (a) (Left panel) Crystal structure of CIPS and the approaches to switch the polarization. The polarization direction is indicated by the blue arrows. (Right panel) The corresponding Landau–Ginzburg–Devonshire double well models for ferroelectric phase and polarization switching process. (b) The PFM hysteresis loops and (c) the spontaneous ferroelectric domains from a 14 nm thick CIPS flake.
reports of electric poling in CIPS, electric field writing does not guarantee effective switch of all the polarizations as indicated by the poor quality of artificially poled domains.

The key to flexoelectric control of the electric polarization in ferroelectrics is to apply large enough strain gradients, which scale inversely with the dimensionality and the size of materials. Benefitting from the flexural out-of-plane bending mode of ultrathin 2D materials, the giant strain gradients can be introduced in regions with high curvature. Therefore, corrugating the 2D CIPS at nanoscale is a good scenario. As summarized in Figure 2a, we developed a method to create rippled ultrathin CIPS on gold coated polydimethylsiloxane (PDMS) through the combination of substrate strain engineering and the all-dry transfer technique. Details of the corrugating process are described in Supporting Information. With this method, we realized the formation of large area rippled CIPS thin flakes with lateral size at around 195 μm (see the optical image in Figure 2b). The polarization states of selected regions with different thicknesses are revealed by the PFM results as shown in the insets of Figure 2b and Figure S6. From the PFM results, we found ordered stripe domains with extremely high uniformity. The formation of uniform stripe ferroelectric domains suggests that the polarization of the entire large area CIPS thin flake can be effectively modulated by the substrate strain engineering at nanoscale. Importantly, artificial domain formation in 2D CIPS via the flexoelectric effect is valid even at scales as large as hundreds of microns.

We next investigate the relationship between the polarization state and the strain gradients (\(\partial u/\partial z\)). Figure 3a shows the topography of a periodic rippled CIPS with PFM contact mode under low loading force (60 nN). We found two regions with the thicknesses identified to be 4 nm (marked by the green line) and 22 nm (marked by the black line), respectively. By examining the piezoresponse from a single periodic area including both the upward and downward bending, the flexoelectric control on polarization is exclusively confirmed by the observation of domain walls with vanished PFM amplitude and the clear 180° phase contrast between domains as presented in Figure 3b,c, respectively. The boundary in PFM phase image (i.e., domain wall) is consistent with the inflection points in the topography image (see Figure S7). It must be emphasized here, relative to the continuously changing topography, the two plateaus in the phase line profile and the rapid switching behavior imply that the measured PFM phase is not from the crosstalk of surface topography. The optical image and the PFM results of the entire CIPS thin flake are shown in Figure S8. From the PFM results, we clearly observe that the artificial stripe domains (domain walls) were achieved of the entire sample. Because the flexoelectric modulation relies on substrate strain transfer, it is necessary to check the adhesion between the CIPS and the PDMS substrate. Therefore, we extracted the line profiles of height perpendicular to the rippled structure. As shown in Figure 3d, the rippled structure has a near-symmetric double-arc geometry of upward and downward bending. In the region with CIPS samples, there is an offset change in height, which indicates the thickness of the CIPS samples. Meanwhile, the identical depths of the substrate and the samples indicate the good adhesion of the CIPS thin flakes to the substrate. Moreover, we carried out the topography test in tapping mode.
From the observed tomography, the corrugated periodic structure in CIPS can be simplified into an arch model (see schematic in Figure 3e) by considering the sample bending nature of the flexoelectric control. The geometry parameters of this model are obtained from the in situ morphology measurements. For CIPS thin flakes with a certain thickness \(d\), upon bending, the upper part experiences tensile strain, while the lower part undergoes compressive strain. Thus, the strain gradient \(\partial u/\partial z\) is perpendicular to the surface and can be written as\(^{44}\)

\[
\frac{\partial u}{\partial z} \sim \frac{u_1 - u_2}{d} = \frac{(R + \frac{1}{2})\frac{1}{2} - l_0}{l_0} - \frac{(R - \frac{1}{2})\frac{1}{2} - l_0}{l_0} = \frac{1}{R} \tag{1}
\]

where \(u_1\) and \(u_2\) are the in-plane strain of the upper surface and the lower surface respectively, \(l_0\) is the original length of the sample, and \(R\) is the ideal radius of curvature of the bent sample. From eq 1, the strain gradient \(\partial u/\partial z\) is inversely proportional to \(R\), which can be calculated by the Pythagorean theorem as

\[
R = \frac{h^2 + \left(\frac{1}{2}\right)^2}{2h} \tag{2}
\]

where \(h\) and \(t\) are the half of the wrinkle depth and the half of the periodicity. From the height profile in Figure 3d, the \(h\) and \(t\) are found to be 50 and 600 nm, respectively. In this case, \(R\) is calculated to be 925 nm, and \(\partial u/\partial z\) is as large as \(1.08 \times 10^6\) m\(^{-1}\). Compared with previous studies of mechanical bending in bulk materials at macroscopic scale where the strain gradient is usually less than 0.1 m\(^{-1}\),\(^{1,5,33,34}\) our result achieves a strain gradient of \(10^6\) m\(^{-1}\). Although the applied strain gradient is giant in this study, the ultrathin CIPS samples remain intact other than collapse. This is benefited from the unique near-zero Poisson ratio found in CIPS,\(^{55}\) so there is almost no out-of-plane strain in our bending geometry. Meanwhile, the in-plane strain in CIPS thin layers (the top and the bottom) is around \(\pm 1\%\).

With the quantified strain gradients, we can estimate the value of effective flexoelectric field, \(E_{\text{flexo}}\). The flexoelectric field can be expressed as\(^{33,43,44}\)

\[
E_{\text{flexo}} = \frac{P_{\text{flexo}}}{\varepsilon_0 \varepsilon_i} = \frac{1}{\varepsilon_0 \varepsilon_i} \left(\frac{\partial u}{\partial z}\right) \tag{3}
\]

where \(\varepsilon_0\) is the permittivity of free space and \(\varepsilon_i\) is relative dielectric permittivity, \(P_{\text{flexo}}\) is the polarization induced by flexoelectricity, and \(\mu\) is the flexoelectric coefficient. According to Tagantsev’s phenomenological studies of the flexoelectric effect in crystalline materials, \(\mu\) can be approximately expressed as\(^{33,34}\)

\[
\mu \sim \chi \frac{e}{a} \tag{4}
\]

where \(\chi\) is the dielectric susceptibility \((\chi = \varepsilon_r - 1 \approx \varepsilon_r)\), \(e\) is the electron charge, and \(a\) is the lattice constant. For CIPS, the \(\varepsilon_r\) is 40 and \(a\) is \(6 \times 10^{-10}\) m.\(^{32}\) We have the flexoelectric coefficient \(\mu\) to be 10.8 nC/m. Therefore, the flexoelectric field \(E_{\text{flexo}}\) in the rippled structure is around \(3 \times 10^5\) V/cm. The strength of

Figure 3. Quantification of the flexoelectric effect in 2D CIPS. (a) Topography image of the rippled CIPS thin flake. Zoomed PFM amplitude (b) and phase (c) images of one period including both upward and downward bending thin CIPS as indicated in the white square region in (a). The insets show the corresponding lateral profiles of amplitude and phase. (d) Selected line profiles of height derived from (a). (e) Simplified arch model for the flexoelectric control of polarization in 2D CIPS. The parameters such as ideal radius of curvature (R), sample thickness (d), wrinkle depth (2h), periodicity (2t), and original sample length (l0) can be directly obtained from panel d.

(see Figure S9), in which the same offset changes in height are observed, which guarantees the transfer of the strain.
the flexoelectric field is comparable to the coercive field of CIPS nanoflakes extracted from the hysteresis loops measurement (∼3.5 × 10^5 V/cm) and in a previous report. It further proves the validity of flexoelectric modulation on the electric polarizations of CIPS in this study. Furthermore, it should be pointed out that the flexoelectric coefficients μ of ferroelectric materials is temperature dependent and should increase largely near the Curie temperature Tc.56 Because the Tc of CIPS is ∼315 K, which is close to the room temperature, the flexoelectric coefficients μ and the flexoelectric field Eflexo in our bending geometry under ambient conditions may be much larger than we estimated.

The geometry-induced flexoelectric effect in 2D CIPS can be understood through the distorted LGD double-well potential model. As a phenomenological theory, it is often employed to qualitatively explain the flexoelectric effect in ferroelectrics. Here, the potential energy profiles (PEP) are quantificationally obtained for CIPS system based on first-principle calculations as shown in Figure 4a. The details of calculation methods and models are given in Supporting Information. For both the flat and bended CIPSs, the migration barriers of Cu⁺ from one surface to the other surface are calculated (see Figure 4a and Figure S11). It is found that the PEP of the flat CIPS has a symmetric double well for the migration of Cu⁺ (see Figure S11); the PEP of the bended CIPS also has a double-well structure but is asymmetric (see Figure 4a). Obviously, it is the strain gradients that break the symmetry of potential energy surface. These calculated results are consistent with the phenomenological theory. It is worth noting that in bended CIPS the migration barrier of Cu⁺ from the contraction surface to stretched surface is much smaller than that between upper and lower surfaces in flat CIPS.

The distorted LGD double-well potential model can be verified through the ferroelectric switching behavior of rippled
CIPS nanoflakes via single electric poling measurements. Figure 4b shows the hysteresis loops from the downward and upward bending areas of a 14 nm thick CIPS, respectively. Because of the symmetrical geometry, downward and upward bending regions should have the same coercivity. The coercive field which is equal to the half-width of the hysteresis loop was found to be around $3.7 \times 10^3$ V/cm at both of downward and upward bending regions, which is close to the value we estimated above. Importantly, the hysteresis loops of downward/upward bending regions are entirely shifted to the negative/positive voltage range accordingly. This result suggests that the degenerate electric polarizations in CIPS are not stable in the bending state. Only either up or down electric polarization can be stabilized subject to the bending direction, which is the manifestation of the flexoelectric effect. When the flexoelectric field induced by strain gradients is parallel to the ferroelectric polarization, it could increase the required external coercive voltage. On the contrary, the flexoelectric field would decrease the required external coercive voltage.

Finally, we show that the stripe domains in 2D CIPS can be effectively tuned in density with the developed substrate strain engineering technique. Controlled arrays of domains in ferroelectrics are important for the practical applications such as nonlinear optics, anomalous photovoltaic effect, and so forth. In this study, the stripe domains in CIPS are controlled by the periodicity of the rippled substrate. By adjusting the periodicity of the rippled substrate (detailed in Supporting Information), we generated different stripe domains with periodicities of 530, 750, and 1200 nm, respectively, as shown in Figure 5a–c (the corresponding topography and PFM amplitude image is shown in Figure S12). It should be noted that although the depth of the ripples changed along with the periodicity, the corresponding strain gradients do not change drastically and remain at the order of $1 \times 10^6$ m$^{-1}$ which ensures the reversal of the polarization (see Figure S13).

The formation and control of stripe domains in CIPS can be numerically interpreted. We compared the energies with and without stripe domain for the same corrugated structures of CIPS, denoted by $E_{\text{Stripe}}$ and $E_{\text{Nonstripe}}$, respectively. The calculated energy differences ($\Delta E = E_{\text{Stripe}} - E_{\text{Nonstripe}}$) are given in Figure 5e. The structures with and without stripe domain are shown by the sketch in Figure 5d. The degree of bending strain can be depicted by a scale factor $\lambda = 1 - t/l_0$, where $l_0$ and $t$ are the length of flat and corrugated supercell including the same number of unit cells, respectively (see the inset in Figure 5e). This scale factor determines the density of stripe domains. In stripe domains with periodicity of 1200 nm, the corresponding scale factor ($\lambda$) is 6.1%, being in the range of our simulated $\lambda$ values (see Figure 5e). According to the definition of $\Delta E$, the negative values of $\Delta E$ indicate that the formation of stripe domain is more preferred in energy. Furthermore, in the structure with stripe domains the Cu ions always prefer to locate at the stretched surface (see Figure 5d) instead of the contraction surface. The latter case corresponds to a metastable state with a higher energy compared to the former, according to calculations. These polarization behaviors are attributed to the flexoelectric effect of ferroelectric CIPS. The evolution trend of $\Delta E$ along the $\lambda$ (or density) indicates that the relative stability of stripe structures increases with the curvature degree of corrugated CIPS.

In summary, we report the flexoelectric method to artificially generate large-scale stripe domains in 2D ferroelectric CuInP$_2$S$_6$. Giant strain gradient ($\sim 10^6$ m$^{-1}$) at nanoscale is achieved via substrate engineering. The electric polarizations in ultrathin CuInP$_2$S$_6$ are mechanically switched via nanoscale bending. Together with first-principle calculations, the flexoelectric control of ferroelectric polarization in 2D CIPS is verified via distorted LGD double well model. Our work highlights the potential of developing vdW ferroelectrics-based flexible 2D electronics.

### ASSOCIATED CONTENT

#### Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.nanolett.2c00130.

Additional results and details for substrate formation, sample preparation, Raman spectroscopy characterization, PFM characterization, first-principle calculation methods, dependence of strain gradients on the periodicity of domains, polarization of the rippled CIPS thin flake, effect of the strain gradients on the $T_c$ of ferroelectric CIPS, outlook for reconfigurable flexoelectric modulation in 2D CIPS (PDF)

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#### Conflict of Interest

The authors declare no competing financial interest.

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H.Z. conceived the idea and supervised the research. C.C., H.L., and Q.L. prepared the samples, fabricated the devices, and carried out the PFM measurements. C.C., Z.F., and H.Z. analyzed the data and wrote the paper. All authors commented on the manuscript.

Notes
The authors declare no competing financial interest.

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