Improved $\Lambda p$ Elastic Scattering Cross Sections Between 0.9 and 2.0 GeV/c as a Main Ingredient of the Neutron Star Equation of State

J. Rowley
N. Compton
C. Djalali
Krishna P. Adhikari
Old Dominion University, kadhi001@odu.edu
Dilini L. Bulumulla
Old Dominion University, dbulumul@odu.edu

See next page for additional authors

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Original Publication Citation
Rowley, J., Compton, N., Djalali, C. ... Yurov, M., Zhang, J., & Zhao, Z. W. (2021) Improved $\Lambda p$ elastic scattering cross sections between 0.9 and 2.0 GeV/c as a main ingredient of the neutron star equation of state. Physical Review Letters, 127(27), 1-7, Article 272303. https://doi.org/10.1103/PhysRevLett.127.272303

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Authors
J. Rowley, N. Compton, C. Djalali, Krishna P. Adhikari, Dilini L. Bulumulla, Mohammad Hattawy, Sebastian E. Kuhn, Pushpa Pandey, Yelena Prok, M. Yurov, J. Zhang, Z. W. Zhao, et al., and CLAS Collaboration
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J. Rowley,35 N. Compton,35 C. Djalali,35 K. Hicks,35 J. Price,2 N. Zachariou,47 K. P. Adhikari,36 W. R. Armstrong,1 H. Atac,41 L. Baashen,13 L. Barion,17 M. Bashkanov,47 M. Battaglieri,42 I. Bedlinskiy,31 F. Benmokhtar,10 A. Bianconi,45,22 L. Biondo,19,16,29 A. S. Biselli,1 M. Bondi,19 F. Bosso,2 S. Boiarinov,42 W. J. Briscoe,15 W. K. Brooks,43 D. Bulumulla,36 V. D. Burkert,42 D. S. Carman,42 J. C. Carvajal,13 A. Celentano,19 P. Chatagnon,23 V. Chesnokov,19 T. Chetry,30 G. Ciullo,17,12 L. Clark,46 P. L. Cole,27 M. Contalbrigo,17 G. Costantini,45,22 V. Crede,14 A. D’Angelo,20,38 N. Dashyan,51 R. De Vita,19 M. Defurse,6 A. Deur,42 S. Diehl,37,8,40 R. Dupré,23 H. Egiyan,42,32 M. Ehrhart,1 A. El Alaoui,43 L. El Fassi,30,1 P. Eugenio,14 G. Fedotov,39 S. Fegan,47,7,50 A. Filippi,21 A. Fradi,23 G. Gavalian,42,36 F. X. Girod,42,6 D. I. Glazier,46 A. Golubenko,39 R. W. Gothe,40 K. Griffioen,50 L. Guo,13 K. Hafidi,1 H. Hakobyan,43,51 M. Hattawy,36 T. B. Hayward,8 D. Heddle,7,42 A. Hobart,23 M. Holtrup,32 Y. Ilieva,40 D. G. Ireland,46 E. L. Isupov,39 D. Jenkins,48 H. S. Jo,26 K. Joo,8 D. Keller,9,35 A. Khanal,13 M. Khandaker,34 A. Kim,8 I. J. D. MacGregor,14 N. Markov,42,8 L. Marsicano,17 G. Niculescu,25 T. R. O’Connell,8 M. Osipenko,19 A. I. Ostrovskiy,14 P. Pandey,36 M. Paolone,33 L. L. Pappalardo,17,12 E. Pasyuk,42 O. Pogorelko,31 Y. Prok,36,49 T. Reed,13 M. Ripani,19 J. Ritman,24 A. Rizzo,20,38 G. Rosner,46 F. Sabatier,6 C. Salgado,34 A. Schmidt,15 R. A. Schumacher,4 Y. G. Sharabian,42 U. Shrestha,3 D. Sokhan,46 O. Soto,1 N. Sparveris,47 I. I. Strakovsky,15 S. Strauch,48 R. Tyson,46 M. Ungaro,42,8 L. Venturelli,45,22 H. Voskanyan,31 A. Vossen,42 E. Voutier,23 D. P. Watts,37 K. Wei,1 X. Wei,42 R. Wishart,46 M. H. Wood,3,40 B. Yale,50 M. Yurov,26 J. Zhang,49,36 and Z. W. Zhao9,40

(CLAS Collaboration)

1Argonne National Laboratory, Argonne, Illinois 60439, USA
2California State University, Dominguez Hills, Carson, California 90747, USA
3Canisius College, Buffalo, New York, USA
4Carnegie Mellon University, Pittsburgh, Pennsylvania 15213, USA
5Catholic University of America, Washington, D.C. 20064, USA
6IRFU, CEA, Université Paris-Saclay, F-91191 Gif-sur-Yvette, France
7Christopher Newport University, Newport News, Virginia 23606, USA
8University of Connecticut, Storrs, Connecticut 06269, USA
9Duke University, Durham, North Carolina 27708-0305, USA
10Duquesne University, 600 Forbes Avenue, Pittsburgh, Pennsylvania 15282, USA
11Fairfield University, Fairfield Connecticut 06824, USA
12Università di Ferrara, 44121 Ferrara, Italy
13Florida International University, Miami, Florida 33199, USA
14Florida State University, Tallahassee, Florida 32306, USA
15The George Washington University, Washington, D.C. 20052, USA
16INFN, Sezione di Catania, 95123 Catania, Italy
17INFN, Sezione di Ferrara, 44100 Ferrara, Italy
18INFN, Laboratori Nazionali di Frascati, 00044 Frascati, Italy
19INFN, Sezione di Genova, 16146 Genova, Italy
20INFN, Sezione di Roma Tor Vergata, 00133 Rome, Italy
21INFN, Sezione di Torino, 10125 Torino, Italy
22INFN, Sezione di Pavia, 27100 Pavia, Italy
23Université Paris-Saclay, CNRS/IN2P3, IJCLab, 91405 Orsay, France
24Institut für Kernphysik (Juelich), 52425 Juelich, Germany
25James Madison University, Harrisonburg, Virginia 22807, USA
26Kyungpook National University, Daegu 41566, Republic of Korea
27Lamar University, 4400 MLK Boulevard, P.O. Box 10046, Beaumont, Texas 77710, USA
28Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA
29Università degli Studi di Messina, 98166 Messina, Italy

0031-9007/2021/127(27)/272303(7) 272303-1 Published by the American Physical Society
Strange matter is believed to exist in the cores of neutron stars based on simple kinematics. If this is true, then hyperon-nucleon interactions will play a significant part in the neutron star equation of state. Yet, compared to other elastic scattering processes, there is very little data on $\Lambda-N$ scattering. This experiment utilized the CEBAF Large Acceptance Spectrometer (CLAS) detector to study the $\Lambda p \rightarrow \Lambda p$ elastic scattering cross section in the incident $\Lambda$ momentum range 0.9–2.0 GeV/$c$. These are the first data on this reaction since the 1970s. The new cross sections have significantly better accuracy and precision than the existing world data, and the techniques developed here can also be used in future experiments.

DOI: 10.1103/PhysRevLett.127.272303

The mass and radius of a neutron star are important parameters to determine its equation of state (EOS) [1]. There is an ongoing debate about the presence of hyperons in the core of neutron stars. If hyperons are present in the core, this can soften the EOS [2], yet a stiffer EOS is needed in the core of neutron stars. If hyperons are present in the core, this can soften the EOS [2], yet a stiffer EOS is needed in the core of neutron stars. Then, theorists may use these results to constrain the $\Lambda N$ potential and hence its effect on the EOS.

Nucleon-nucleon ($NN$) scattering is perhaps the most well studied of all nuclear reactions. However, less is known about the scattering of hyperons ($\Lambda$ or $\Sigma$ baryons) from the proton. Previous data for the scattering of hyperons from the nucleon dates back to the bubble chamber era of the 1960s and 1970s [7,8]. These experiments ranged from tens of events to a few hundred spread across multiple momentum bins. The experiment with the greatest statistics is from [9] with a total of 584 events spread over 12 momentum bins. The paucity of data for $\Lambda N$ scattering is due to the difficulty of creating a $\Lambda$ beam. The decay parameter for $\Lambda$ particles is $c\tau \sim 7.89$ cm, which is too short for a modern beamline. Hence, data for $\Lambda N$ scattering are very limited in comparison with other elastic scattering processes [10], such as $NN$, $KN$, or $\pi N$. The present results in this work improve on the existing world data.

The data for this work were collected during the g12 experiment, which was conducted at the Continuous Electron Beam Accelerator Facility (CEBAF) using the
Large Acceptance Spectrometer (CLAS) at the Thomas Jefferson National Accelerator Facility [11]. The experiment consisted of a tagged photon beam incident on a liquid-hydrogen target, 40 cm long by 4 cm in diameter. The photon beam energy ranged from 1.2 to 5.4 GeV and was determined using the CLAS electron tagger system [12].

The CLAS detector was based on a toroidal magnetic field consisting of six independent sectors separated by the superconducting magnet coils. Each sector included three regions of drift chambers (DC) to measure the charged particle trajectories [13]. Plastic scintillators surrounded the regions of drift chambers (DC) to measure the charged particles and measure their four momenta. Further detector details can be found in Ref. [15].

Observation of \( \Lambda p \to \Lambda p \) elastic scattering with the CLAS detector is a two-step process. The reaction proceeds as follows, which is further illustrated in Fig. 1:

\[
\gamma p_{\text{tgt}} \to [K^+]\Lambda; \quad \Lambda p \to \Lambda' p' \to \pi^- p' p. \tag{1}
\]

Here, the \( \Lambda \) “beam” is provided from the products of the first reaction. Detection of the \( K^+ \), which often decays before reaching the outer part of CLAS, was not required as it was identified using missing mass techniques. The \( \Lambda \) then propagates through the target until it either exits, decays, or scatters with a proton at rest. The recoil proton, \( p' \), was detected directly and the \( \Lambda' \) was detected through its decay, \( \Lambda' \to \pi^- p \), which has a branching ratio of 64%. The decay proton and \( \pi^- \) were directly detected by CLAS, resulting in a fully exclusive measurement.

Final-state particles were detected using standard \( g12 \) techniques [15]. These procedures include timing cuts on the photon and final-state particles, vertex tracing, fiducial region selection, and event trigger efficiency corrections. The electron beam was bunched into buckets 2 ns apart, which produced the bremsstrahlung photons also in 2-ns bunches. The final-state particles were filtered using the DC and TOF scintillator for particle identification. Particle tracks that did not trace back to the target volume were removed. Fiducial cuts were applied, which filtered out data outside the active region of the DC. A Monte Carlo (MC) simulation was done to model the CLAS detector in order to measure the reaction acceptance (discussed below). The simulated events went through the same analysis as the data and included an additional trigger efficiency correction. An intensive study of the trigger was done [16] and is accounted for in the simulation.

The reaction specific analysis required \( \gamma p \to K^+ \Lambda \) events to be isolated. The scattering \( \Lambda' \) was identified from the combined momenta of its decay products, \( p_{\pi^-} + p_p \). These four momenta produced a mass spectrum, shown in Fig. 2(a). The peak at 1.115 GeV/c\(^2\) corresponds to the scattered \( \Lambda' \). The background under the peak is from other photoproduction reactions that have a \( p \) and \( \pi^- \) in the final state. The peak was fit to a Gaussian function, shown by the dashed line, and events within \( \pm 3\sigma \) passed to further

![FIG. 1. Pictorial representation of the reaction inside the liquid-hydrogen target. A two-part reaction occurs where the incident \( \Lambda \) is created at vertex (1), followed by scattering with a proton at rest in the target at vertex (2), before the \( \Lambda' \) decays at vertex (3).](image)

![FIG. 2. Mass spectrum of the detected proton and \( \pi^- \) (top) from the decayed \( \Lambda' \) and the missing mass spectrum of the initial vertex (bottom). The missing mass spectrum (bottom) was plotted after the cut was made around the \( \Lambda' \) mass (top). The total fit, peak plus background, is shown by the solid line. The Gaussian fits, shown by the dashed lines, are for reference only, and are not used in the cross section calculation. The vertical lines frame the data that pass through to the final analysis.](image)
analysis. From the scattered $\Lambda'$ and the other detected proton, the $K^+$ can be identified through the missing four momentum $p_X$:

$$p_X = p_{p'} + p_{tgt} - (p_{\Lambda'} + p_{p'} - p_{tgt}),$$  \hspace{1cm} (2)

where $p_{\Lambda'}$ is for the recoil $\Lambda$, $p_{p'}$ is for the recoil proton, and $p_{tgt}$ is for target proton. There are two $p_{tgt}$ terms above, which come from the two target protons at vertex (1) and (2) in Fig. 1. This four momentum gives the missing mass (MM) spectrum shown in Fig. 2(b) which shows only events for the exclusive reaction $p\gamma \rightarrow K^+\Lambda$, whereas Fig. 2(a) shows inclusive $\Lambda$ production. There is a peak at the mass of the $K^+$, which isolates the first vertex of the two-step process leading to the $\Lambda p \rightarrow \Lambda' p'$ elastic scattering. The peak at the $K^+$ mass was fit to a Gaussian function and a selection was made at $\pm 3\sigma$. The background under the $K^+$ peak comes from a variety of sources, similar to the background under the $\Lambda$ peak shown above. For example, some events may include extra particles which were not detected by CLAS, such as pions that hit the magnet coils. Those events do not form a peak at the $K^+$ mass.

Additional analysis was also required to remove background from the $pp \rightarrow pp$ elastic scattering reaction. This reaction can happen when the $\Lambda$ decays, followed by an elastic scattering of the decay proton. This leads to the same final state that can be misidentified as $\Lambda p \rightarrow \Lambda' p'$ events. Kinematic calculations were used to remove these events. Figure 3 shows the missing mass distribution of the presumed incident $\Lambda$ on the $x$ axis and that of the presumed proton on the $y$ axis, where $X$ is the missing particle. There are prominent bands at the mass of the $\Lambda$ (vertical band) and the mass of the proton (horizontal band). At the intersection of these bands there is significant overlap. This region represents $pp$ elastic scattering events that must be removed. The band to the right of the overlap is due to background from other reactions, such as $\gamma p \rightarrow \pi^+\pi^- p$ followed by $pp \rightarrow pp$ elastic scattering. Data above the dashed line are rejected, reducing the background along with removing the $pp$ elastic events. The same cut is applied to the MC events, so the detector acceptance compensates for any good events cut from the top of the $\Lambda$ distribution.

The $pp$ scattering events were used as a cross check to verify this analysis. Since many of these events were detected, it was possible to also measure the $pp$ elastic scattering cross section, which is well known. This method yielded consistent results with the world data for $pp$ scattering.

With the initial reaction $\gamma p \rightarrow K^+\Lambda$ identified, the incident $\Lambda$ could now be isolated using the missing four momentum:

$$p_X = p_{\Lambda'} + p_{p'} - p_{tgt},$$  \hspace{1cm} (3)

where $p_X$ is for the missing particle, $p_{\Lambda'}$ is for the scattered $\Lambda'$, $p_{p'}$ is for the recoil proton, and $p_{tgt}$ is for the target proton. The missing mass spectrum of Fig. 4(a) shows a prominent peak at the mass of the $\Lambda$, 1.115 GeV/c$^2$. This distribution is plotted using events that pass the above selections of both the scattered $\Lambda'$ and the $K^+$ peaks, after subtraction of the background as explained below.

The energy dependence of the cross section was determined by binning the missing mass spectrum as a function of the incident $\Lambda$ momentum. An example bin is shown in Fig. 4(b). As part of the analysis, the sideband subtraction technique was used to extract the yield. This was done by selecting the data to either side of the $\Lambda'$ peak in Fig. 2(a), such that the cut has the same width as that about the peak. The sideband region should have no scattered $\Lambda$ events, so all the data resulting from sidebands were treated as background and subtracted from the final data. The sideband subtraction provided a first-order estimate of the background and provided a better signal-to-noise ratio to extract a yield of the $\Lambda$ peak. With this method, most of the background was removed from Fig. 4(b), leaving only signal events. The remaining background in Fig. 4(b) was fit to both a flat line and a second order polynomial. The flat background was taken as the nominal fit, while the polynomial acted as a check of the systematic uncertainty in the fit. The signal peak at the mass of the $\Lambda$ was fit to a Gaussian function. The yield was then extracted from the peak fit, integrating the Gaussian in the $\pm 3\sigma$ interval.

To get the acceptance of the detector, a simulation must be done that models the CLAS detector. A custom event generator was used to produce $\Lambda p$ elastic scattering events using existing $K^+\Lambda$ cross sections in order to model a realistic angular dependence [17].

The angular dependence was modeled using the Mandlestam $t$ parameter. We treat the constant that multiplies $t$ in our simulation as a model parameter. By comparing the $t$ dependence of the simulation to the data,
an accurate $\Lambda$ angular distribution was modeled and variations in the $t$ parameter were used to study the systematic uncertainty of the acceptance.

The generated events were passed through a Monte Carlo simulation utilizing the standard GEANT software [18]. The acceptance of the detector for this two-step reaction ranged from ~0.1–2.0% in $\Lambda$ momentum, over a $p_\Lambda$ range of 0.9 to 2.0 GeV/c.

Beam flux calculations were more involved than for typical CLAS experiments. Unlike a photon beam or electron beam that enters the target from one end and is parallel to the beam axis, the $\Lambda$ particles are created throughout the length of the target and have an angular distribution. The luminosity of the $\Lambda$ beam can be calculated by

$$L(p_\Lambda) = \frac{N_A \times \rho_T \times l}{M} \times N_\Lambda(p_\Lambda),$$

where $N_A$ is Avogadro’s number, $\rho_T$ is the mass density of the target, $l$ is the average path length of the $\Lambda$ beam in the target, $M$ is the molar mass of hydrogen, and $N_\Lambda$ is the number of $\Lambda$ particles in the beam with incident momentum $p_\Lambda$. Unlike the photon beam, for the secondary $\Lambda$ beam, the average path length ($l$) and $\Lambda$ flux ($N_\Lambda$) cannot be directly measured.

To calculate the luminosity of the $\Lambda$ beam, a simulation was made that generated $\Lambda$ particles uniformly throughout the length of the target and within the radius of the photon beam. The angular distribution was simulated using known cross sections for the $\gamma p \rightarrow K^+ \Lambda$ vertex [17]. The simulation also must account for $\Lambda$ particles decaying and exiting the side of the target. Once the $\Lambda$ particles were generated with their initial properties such as momentum, energy, vertex position, and lab angle, they were propagated through the target. The probability for particle decay is given by

$$P(x) = \exp \left[ -\frac{M x - x_0}{\tau} \right],$$

where $P(x)$ is the probability that a $\Lambda$ survives to the point $x$ after being created at $x_0$. The momentum of the $\Lambda$ is $p/c = M/\gamma$ (where $c = 1$) and $\tau$ is its lifetime, in order to keep everything in the lab frame where the experiment takes place. The path length was then averaged for each generated particle.

The number of $\Lambda$ particle $N_\Lambda$ can be calculated using

$$\frac{N_\Lambda}{L_\gamma} = \frac{d\sigma}{d\Omega} (2\pi) [\Delta \cos(\theta)],$$

where $L_\gamma$ is the luminosity of the photon beam, and $\theta$ is the center of mass angle of the $K^+$ particle. The $\Lambda$ production cross section $\sigma$ can be calculated from the differential cross section $d\sigma/d\Omega$ by integrating over the range of $\cos(\theta)$ which is kinematically constrained by the momentum of the particles. From Eqs. (4) and (6) together with Eq. (5), the luminosity of the $\Lambda$ beam was calculated.

Cross sections were calculated for a given momentum bin and integrated over the full angular range as

$$\sigma(p_\Lambda) = \frac{Y(p_\Lambda)}{A(p_\Lambda) \times L(p_\Lambda) \times \Gamma},$$

where $Y$ is the yield, $A$ is the acceptance for $\Lambda^+ p$, $L$ is the luminosity of the $\Lambda$ beam, and $\Gamma$ is branching ratio (0.64) [10]. Figure 5 shows the total cross section as a function of the momentum of the incident $\Lambda$ beam. The data from the present analysis, in solid boxes, are compared to existing world data [9,19–24]. The vertical error bars represent statistical uncertainties only.

A study of the systematic uncertainties was done at each stage of the analysis. The largest source comes from the $\Lambda$ beam luminosity calculation and the associated $\gamma p \rightarrow K^+ \Lambda$ cross sections. This systematic uncertainty is estimated at
Variations in cuts made in the analysis, such as cuts on the detail in Ref. [15], was estimated at 8.2%. Variations in cuts was varied in the event generator, which resulted in a angular dependence in the simulation. The angular dependence within the chiral EFT model.

The shaded region at the bottom shows the systematic error. The uncertainty from the beam normalization, described in detail in Ref. [15], was estimated at 8.2%. Variations in cuts made in the analysis, such as cuts on the $\Lambda'$, $\Lambda$, and $pp$ combined to give an additional uncertainty of 8.4%. Other systematic uncertainties include detector-related variation constraints on the detector geometry and target vertex position (2.1%) [11]. The overall systematic uncertainty for the experiment, added in quadrature, is estimated at 17.3%.

The theoretical model predictions for $\Lambda p$ elastic scattering, shown by the curves in Fig. 5, have been extended to 1.4 GeV/c for the purpose of this analysis [26]. Beyond this momentum the theoretical predictions are not reliable. The green band in Fig. 5 is a calculation at next to leading order from chiral effective field theory (EFT) [5]. The derivation of the chiral baryon-baryon potentials for the strangeness sector is done using Weinberg power counting as shown in [5]. The red line represents the range of uncertainty in the calculation. Figure 5 also shows predictions from the well known models of Jülich [27] and Nijmegen [28]. Our results do not follow the predictions of these meson-exchange models, which were not fit to our data, but further adjustment of the model parameters may provide better agreement. Our measurements do, however, fall in the band of the EFT calculation.

For $p_\Lambda > 1.4$ GeV/c, our results trend downward, falling below the older data. However, there are large fluctuations in the older data (for example, the points at 1.5 GeV/c) and some points are averaged over a wide momentum bin. Also, there were no changes to our analysis procedure across the momentum range. Considering these factors together with the higher statistics of the present measurements, the new cross sections are an improvement over the older data.

We also note that the cross section begins to increase around $p_\Lambda = 1.6$ GeV/c. This may be due to the opening of an inelastic channel that affects the elastic cross section, likely the reaction $\Lambda p \rightarrow \Lambda(1520)p$. The threshold for this reaction is at $p_\Lambda = 1.77$ GeV/c, which is a possible explanation for the structure seen in the high momentum range.

To summarize, this experiment was able to improve upon the existing data of $\Lambda p$ elastic scattering in a momentum range of importance to neutron star physics. We achieve the highest statistical measurement (<10%) for this momentum range. This is the first experiment to measure the $\Lambda p$ elastic scattering cross sections in this energy range outside of bubble chamber experiments, all of which were done prior to 1980. The cross sections presented in this Letter have higher accuracy, particularly in the higher momentum range $p_\Lambda > 1.4$ GeV/c, as well as having significantly better precision compared to the existing world data. These results, along with future three-body reaction data such as the $\Lambda$-deuteron interaction, will help constrain the neutron star EOS. Techniques developed here for secondary scattering of hadrons from photoproduction can also be used for future data analysis. Measurements at CLAS using this technique on a deuterium target are in progress [29].

The authors acknowledge the staff of the Accelerator and Physics Divisions at the Thomas Jefferson National Accelerator Facility who made this experiment possible. This work was supported in part by the Chilean Comisión Nacional de Investigación Científica y Tecnológica (CONICYT), by CONICYT PIA Grant No. ACT1413, the Italian Istituto Nazionale di Fisica Nucleare, the French Centre National de la Recherche Scientifique, the French Commissariat à l’Energie Atomique, the United Kingdom Science and Technology Facilities Council (STFC), the Scottish Universities Physics Alliance (SUPA), the National Research Foundation of Korea, and the U.S. National Science Foundation. The Southeastern Universities Research Association operates the Thomas Jefferson National Accelerator Facility for the United States Department of Energy under Contract No. DE-AC05-06OR23177.

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