Superconducting Gap of Pressure Stabilized (Al\textsubscript{0.5}Zr\textsubscript{0.5})H\textsubscript{3} from Ab Initio Anisotropic Migdal–Eliashberg Theory

Pruttipong Tsuppayakorn-aek, Rajeev Ahuja, Thiti Bovornratanaraks,* and Wei Luo

ABSTRACT: Motivated by Matthias’ sixth rule for finding new superconducting materials in a cubic symmetry, we report the cluster expansion calculations, based on the density functional theory, of the superconducting properties of Al\textsubscript{0.5}Zr\textsubscript{0.5}H\textsubscript{3}. The Al\textsubscript{0.5}Zr\textsubscript{0.5}H\textsubscript{3} structure is thermodynamically and dynamically stable up to at least 200 GPa. The structural properties suggest that the Al\textsubscript{0.5}Zr\textsubscript{0.5}H\textsubscript{3} structure is a metallic. We calculate a superconducting transition temperature using the Allen–Dynes modified McMillan equation and anisotropic Migdal–Eliashberg equation. As result of this, the anisotropic Migdal–Eliashberg equation demonstrated that it exhibits superconductivity under high pressure with relatively high-\(T_c\) of 55.3 K at a pressure of 100 GPa among a family of simple cubic structures. Therefore, these findings suggest that superconductivity could be observed experimentally in Al\textsubscript{0.5}Zr\textsubscript{0.5}H\textsubscript{3}.

INTRODUCTION

Motivated by the discovery of the intermetallic superconductor Nb\textsubscript{3}Sn in 1954, its superconducting transition temperature (\(T_c\)) was found by Matthias et al. to be \(T_c\) of 18 K. In addition, in 1973, the intermetallic compound Nb\textsubscript{3}Ge was reported by Gavaler to superconduct with \(T_c\) up to 22 K. The superconductivity of intermetallics has encountered high \(T_c\), but their \(T_c\) cannot overtake the boiling point of nitrogen at 77 K. In 1968, the work of Ashcroft was beginning to reveal that hydrogen became a metallic state. Following this prediction, hydrogen in a metallic state can achieve a high \(T_c\) as suggested by Gilman. Interestingly, the phenomenon of the superconductivity of metallic hydrogen can be described by the Bardeen–Cooper–Schrieffer (BCS) theory based on phonon-mediated superconductivity. In 2004, the potential of hydrogen further indicated that it is a dominant component for alloys of metallic hydrogen because of the considerable increase in the electron–phonon coupling (EPC).

In a great success for BCS theory and the prediction of Ashcroft, the discoveries of high \(T_c\) for metal hydrides have since been experimentally observed; moreover, metal hydrides have been theoretically predicted to have high \(T_c\). Recently, an isostructural family of Al\textsubscript{15} was reported in AlH\textsubscript{3} and ZrH\textsubscript{3}.

It is interesting to note that both AlH\textsubscript{3} and ZrH\textsubscript{3} are isostructural to Nb\textsubscript{3}Sn and Nb\textsubscript{3}Ge with \(Pm\overline{3}n\) symmetry. Also, these structures turn out to be superconductors at high pressure. To clarify, AlH\textsubscript{3} attracted interest because of a discrepancy between theoretical and experimental findings. It should be mentioned that the contradiction of superconductivity in AlH\textsubscript{3} was investigated by Abe and was revealed to superconduct at pressures above 100 GPa. Also, its \(T_c\) is theoretically predicted to be 28.5 K at a pressure of 105 GPa and 24 K at a pressure of 110 GPa. For ZrH\textsubscript{3}, very recently, it was explored in detail theoretically by predicting a crystal structure at 1 atm and 50 and 100 GPa. As a result of this, the \(Pm\overline{3}n\) symmetry is thermodynamically stable up to at least 100 GPa. Besides, ZrH\textsubscript{3} was successfully synthesized in detail experimentally in diamond anvil cells by two different reaction routes. These findings tempt one to examine its \(T_c\). In short, the \(T_c\) of ZrH\textsubscript{3} is reported to be 6.4 K at a pressure of 40 GPa according to the aforementioned experimental findings and recent extensive studies. It is also worth paying attention to the prospective structure because it has suitable abilities to carry out superconductivity of Al/Zr-substituted metal trihydride at high pressure. In particular, the structure effectively predicted a \(T_c\) within the same theoretical framework employed here.

Therefore, in this paper, Al/Zr-substituted metal trihydride is investigated by using a cluster expansion (CE) based on density functional theory. Equally important, as mentioned...
above, both AlH$_3$ and ZrH$_3$ found that the $Pm\bar{3}n$ symmetry is theoretically stable at high pressure. Thus, we start by calculating a pressure of 100 GPa. As a consequence, Al/Zr-substituted metal trihydride can be obtained from the ground-state structure. With this in mind, Matthias' sixth rule paves the way for a successful search for new superconducting materials, and one of them indicated the first rule that high symmetry is good and cubic symmetry is the best for example, sulfur hydride SH$_3$ has the $Im\bar{3}m$ symmetry with $T_c$ of 203 K at a pressure of 155 GPa$^{9,27,28}$ and lanthanum hydride LaH$_3$ the $Fm\bar{3}m$ symmetry with $T_c$ of 260 K at a pressure of 185 GPa$^{29−31}$. Herein, all compositions predict up to 92 structures, and we find that Al$_{0.5}$Zr$_{0.5}$H$_3$ is a simple cubic structure with $Pm\bar{3}$ symmetry. Following this, Al$_{0.5}$Zr$_{0.5}$H$_3$ does not decompose into the composition of AlH$_3$ and ZrH$_3$. This in turn implies that Al$_{0.5}$Zr$_{0.5}$H$_3$ is thermodynamically and dynamically stable favored over the AlH$_3$ and ZrH$_3$ structures. Yet, in this paper, the $T_c$ is carried out by the anisotropic Migdal–Eliashberg equation$^{32,33}$. Consequently, it will lead to the discovery of quite interesting Al$_{0.5}$Zr$_{0.5}$H$_3$. The findings suggest that the $T_c$ of Al$_{0.5}$Zr$_{0.5}$H$_3$ reaches 55.3 K at the pressure of 100 GPa.

**COMPUTATIONAL DETAILS**

The search for the structures of Al/Zr-substituted metal trihydride was performed by CE, based on first-principle calculations. Substitution of the atomic type can be obtained from the CE method, indicating the energy of cluster expansion as a function of occupation. Al/Zr-substituted metal trihydride was explored by CE with the MIT Ab initio Phase Stability (MAPS) code$^{35}$ as implemented in the Alloy-Theoretic Automated Toolkit (ATAT)$^{35}$ with the combined Quantum Espresso (QE) package$^{36}$ which plays a considerable role in the exploration of the derived ground-state structure. The plane-wave energy cutoff of 60 Ry and k-point meshes with about 4000 k-points were used. A plane-wave basis set up to cutoff energy of 500 eV and an initial Brillouin-zone (BZ) sampling grid of 8 × 8 × 8 k-points were used for the partial electronic band structure and density of state as implemented in the Vienna ab initio simulation package (VASP)$^{37}$. The zero-point energy of nuclei (ZPE) is estimated within the harmonic approximation, as employed with the use of PHONOPY package$^{38}$ with the combined QE package. For electron–phonon and the spectral function calculations a plane-wave energy cutoff of 60 Ry was used. The dense k-point mesh containing all k and k+q grid points was used. The subsequent electron–phonon and spectral function calcula-
tions depended on the k-point part because it covered the grid of the q-point. The calculations were computed in the first BZ on 16 × 16 × 16 k-points mesh and 4 × 4 × 4 q-meshes, showing that it is sufficient to produce accurate electron–phonon coupling. Computational details of the electron–phonon and spectral function calculations were successfully reported in the theoretical studies.\textsuperscript{39} The Allen–Dynes modified McMillan (ADM) equation\textsuperscript{39} was exploited with the effective Coulomb pseudopotential parameter $\mu^*$ of 0.10–0.13 as follows

$$T_c = f_1 \frac{\omega_{\log}}{1.2} \exp \left[ -\frac{1.04(1 + \lambda)}{\lambda - \mu^*(1 + 0.62\lambda)} \right]$$

(1)

where $\omega_{\log}$ is the logarithmic average of the spectral function, $\lambda$ is the total electron–phonon coupling strength, and $f_1$ and $f_2$ are the correction factors:

$$f_1 = \left\{ 1 + \frac{\lambda}{2.46(1 + 3.8\mu^*)^{1/2}} \right\}^{1/3}$$

(2)

$$f_2 = 1 + \frac{\lambda^2(\omega_1/\omega_{\log} - 1)}{\lambda^2 + [1.82(1 + 6.3\mu^*)^2(\omega_1/\omega_{\log})]^2}$$

(3)

More details about these equations are described in ref 39. In this methodology, the calculations were performed by using density functional theory (DFT). We used the ultrasoft pseudopotentials\textsuperscript{30} and the generalized gradient approximation of the Perdew–Burke–Ernzerhof (GGA-PBE) functional\textsuperscript{41} to describe the core and valence electrons as well as the conjugate gradient scheme, as implemented in the QE package.\textsuperscript{36} We calculated the EPC within the density functional perturbation theory.\textsuperscript{30,42} We investigated the nature of the superconducting gap by using anisotropic Migdal–Eliashberg (ME) formalism\textsuperscript{52,53} with the electron–phonon coupling using the Wannier functions (EPW) software.\textsuperscript{43,44} Generating maximally localized Wannier functions was used, as implemented in the WANNIER90 code.\textsuperscript{28} The dense k-points mesh contained all k and k+q grid points were used. The calculates used a homogeneous fine k-point and q-point grid containing 60 points, respectively, indicating that the calculations depended on the k-point part due to it covered the grid of q-point. We have studied the phonon-mediated superconductivity, and an effective Coulomb potential $\mu^*$ = 0.10 was used for solving the anisotropic ME equations

$$Z(k, i\omega_n) = 1 + \frac{\pi T}{N_0\omega_n} \sum \frac{\alpha_{\kappa}^*}{\sqrt{\alpha_{\kappa}^2 + \Delta^2(k, i\omega_n)}} \lambda(k, \kappa, n - n') \delta(\epsilon_{\kappa})$$

(4)

$$Z(k, i\omega_n) \Delta^2(k, i\omega_n) = \frac{\pi T}{N_0} \sum \frac{\Delta(k, i\omega_n)}{\sqrt{\alpha_{\kappa}^2 + \Delta^2(k, i\omega_n)}}$$

(5)

$$\left[ \lambda(k, \kappa, n - n') - N_F V(k, \kappa) \right] \delta(\epsilon_{\kappa})$$

$$\lambda(k, \kappa, \omega) = \int_0^\infty \omega d\omega \frac{2\omega}{(\omega_1 - \omega_0)\omega} + \omega^2 \alpha^2 F(k, \kappa, \omega)$$

(6)

The $T_c$ can be obtained from the superconducting gap $\Delta(i\omega_n)$ when numerically solving the ME equation.

### RESULTS AND DISCUSSION

As first step, we aimed to search the Al/Zr-substituted metal trihydride structure at the pressure of 100 GPa. As mentioned previously, the CE was carried out for prediction of the ground-state structure, based on the DFT. In detail, a substitute for an atomic type was generated for up to 92 structures. All structures were confirmed by the ground-state energy based on the DFT. With this result, we found that the Al$_0.5$Zr$_0.5$H$_3$ structure is energetically more stable than the AlH$_3$ and ZrH$_3$ structures as shown in Figure 1a. Following this, we considered that the formation energy in the Al$_0.5$Zr$_0.5$H$_3$ structure might not be enough for confirmation of the structural stability. We further investigated the thermodynamic stability by including the PV term; this in turn implies that the thermodynamic stability of the Al$_0.5$Zr$_0.5$H$_3$ structure is demonstrated by enthalpy. Moreover, the hydrogen is the light mass and it exhibits high frequency; therefore, the inclusion of ZPE plays an important role for examination of a stable structure. In the same way, our enthalpy calculations included the ZPE effect in the final calculations of a convex hull of different pressures. This is evident from Figure 1b, where it seems that the Al$_0.5$Zr$_0.5$H$_3$ structure is thermodynamically stable at the pressure of 100 GPa. Beyond 100 GPa up to 200 GPa, it shows that the Al$_0.5$Zr$_0.5$H$_3$ structure is thermodynamically stable up to at least 200 GPa. Additionally, it should be noted that type of high-pressure formation route can be demonstrated by considering A + B → C, where A and B are reactants and C is the resultant. At this point, we defined A and B as AlH$_3$ and ZrH$_3$; therefore, we can obtain the result from the high-pressure formation route, i.e., (0.5)AlH$_3$ + (0.5)ZrH$_3$ → Al$_0.5$Zr$_0.5$H$_3$. The optimized structural parameters for the Al$_0.5$Zr$_0.5$H$_3$ structure are $a = b = c = 3.2773$ Å, with Al atoms located at the 1b symmetry site (0.000, 0.000, 0.000), Zr atoms located at the 1a symmetry site (0.500, 0.500, 0.500), and H atoms located at the 6g symmetry site (0.500, 0.000, 0.739); see Figure 1c. Apart from this, it should be mentioned that the space group of the AlH$_3$ and ZrH$_3$ structures is an isostructural of the Nb$_2$Sn structure with $Pm\bar{3}n$ symmetry, which are known crystal structures in the previously reported A15-group, as shown in Figure 1d. Subsequently, as mentioned in optimized structural parameters, our results manifested that a space group of the crystal structure of Al$_0.5$Zr$_0.5$H$_3$ is $Pm\bar{3}n$ symmetry. With this, the Al$_0.5$Zr$_0.5$H$_3$ structure has lower symmetry than the AlH$_3$ and ZrH$_3$ structures through structural relaxation. This in turn implies that structural relaxation reduces from $Pm\bar{3}n$ symmetry to $Pm\bar{3}$ symmetry.

Regarding the electronic properties in the Al$_0.5$Zr$_0.5$H$_3$ structure, according to the aforementioned theoretical findings,\textsuperscript{25} the existence of superconductivity in aluminum hydrides showed that a key factor is the contribution of the density of state. As demonstrated in Figure 2, we now move to the characteristic of the partial electronic structure and the partial density of state (PDOS) of the $Pm\bar{3}$ structure, and the present results show that the $Pm\bar{3}$ structure displays the metallicity at the pressure of 100 GPa. It found that the band dispersions are displayed by the weaving of the up-running bands from below $E_F$ and down-running bands above $E_F$. It is a remarkable result that shows the valence and conduction bands are crossed around the Fermi level. Also, it is interesting to note that Zr substitution onto Al exhibits hybridization with the Al and H atoms, showing the PDOS. Here again, as already
mentioned in the work of Abe,\textsuperscript{23} the dominant feature of the occupied electron around the Fermi level toward the metallicity, supporting the \( T_c \). As a result, our calculation manifested that the total DOS at the Fermi energy is larger in the Al\(_{0.5}\)Zr\(_{0.5}\)H\(_3\) structure because of the dominant feature of the occupied electron of Zr around the Fermi level. To elucidate whether electronic PDOS at the Fermi level plays a crucial role in determining the corresponding superconducting behavior of the Al\(_{0.5}\)Zr\(_{0.5}\)H\(_3\) structure, we must further consider their local density of states (LDOS), which is defined as

\[
N(E, \mathbf{r}) = \sum_n \int \frac{d^3k}{(2\pi)^3} \delta(E - \epsilon_{nk}) |\psi_{nk}(\mathbf{r})|^2
\]

(7)

where \( \psi_{nk}(\mathbf{r}) \) and \( \epsilon_{nk} \) indicate the Kohn–Sham eigenfunctions and eigenvalues of the system, respectively. As determined at the Fermi level, LDOS is a tool by which the degree of the electron–phonon coupling effect in a given material, directly giving rise to Cooper pairing, is visualized,\textsuperscript{47,48} and the electron–phonon coupling effect will be discussed shortly later.

As mentioned earlier, the role of total DOS is a key factor in determining the electron–phonon coupling and superconducting transition temperature. It is also interesting to consider the lattice parameter and bond length with increasing pressure.

The structural morphology has been compressed from 100 to 200 GPa. It showed that the lattice parameter decreased significantly by approximately 3.2773 to 3.0935 Å leading to decreasing a bond length. To explain, the bond length environment of the Al\(_{0.5}\)Zr\(_{0.5}\)H\(_3\) structure displayed that \( d_{\text{Al-H}}, d_{\text{Zr-H}}, \) and \( d_{\text{H-H}} \) decreased moderately from 1.8173 to 1.7075 Å, from 1.8473 to 1.7523 Å, and from 1.5714 to 1.4465 Å, respectively, as shown in Figure 3. As a consequence, the remarkable result of total DOS showed that it declined steeply from 0.4388 to 0.4054 state/eV. To support the electron–phonon coupling of the Al\(_{0.5}\)Zr\(_{0.5}\)H\(_3\) structure, it might be worth trying to estimate the electron–phonon coupling constant; namely, it is found to be possible that the electron–phonon coupling constant decreased with increasing pressure.

We now move to discuss the dynamical stability of the Al\(_{0.5}\)Zr\(_{0.5}\)H\(_3\) structure. Our calculations showed that the Al\(_{0.5}\)Zr\(_{0.5}\)H\(_3\) structure is dynamically stable from 100 to 200 GPa as the phonon frequencies are all positive, as shown in Figure 4a–c. These findings indicate the Al\(_{0.5}\)Zr\(_{0.5}\)H\(_3\) structure can synthesize. What’s more, it is interesting to note that the magnitude of the electron–phonon coupling constant, which represents a solid circle, can be decomposed into the phonon dispersion. Following this, the electron–phonon coupling constant exhibited the major contribution from the intermediate optical phonon mode to the optical phonon mode. This is in fact in line with the spectral function \( \alpha^2F(\omega) \), as shown in Figure 4d–f. Here, it showed that the Eliashberg spectral function contributed slightly in acoustic phonon mode and it contributed mainly in the intermediate optical phonon mode as well as contributed moderately in the optical phonon mode. The solution of the integration of \( \lambda \) displayed that it climbed dramatically in the intermediate optical phonon mode. After that, it remained stable until the optical phonon mode. Then it increased moderately up to the highest phonon frequency of

\[ \text{Pressure (GPa)} \]

\[ \text{Lattice constants (Å)} \]

\[ \text{Bond length (Å)} \]

\[ N(E_F) \]

Figure 3. (Left) Calculated lattice constant and bond length as a function of pressure. (Right) Total density of states at Fermi level as a function of pressure ranging from 100 to 200 GPa.
To further explore the superconductivity of the Al$_3$Zr$_{0.5}$H$_3$ structure, the $T_c$ is carried out by using the anisotropic ME equations. Herein, the anisotropic ME equations have been studied by considering the temperature dependence of the superconducting gap. Consequently, as can be seen in Figure 5, we have shown the superconducting gap at the pressure of 100 GPa. Based on $\mu^* = 0.10$, the superconducting gap closes at the critical temperature of 55.3 K. Likewise, at the pressure of 150 GPa, the superconducting gap displays the temperature evolution, indicating that the gap closes at the critical temperature estimated to be 45 K. With increasing pressure up to 200 GPa, the superconducting gap is likely to close at a critical temperature of 35 K. It should mention that the superconducting gap distribution shows a broad maximum around 4 meV, at which the superconducting gap is nearly zero. Therefore, the superconducting gap can be numerically solved by the anisotropic ME equations at each temperature. Following this, the superconducting gap closes at a critical temperature of 55.3 K, which plotted with the dot line, based on $\mu^* = 0.10$, by using the isotropic ME theory. Likewise, beyond 100 GPa up to 200 GPa, the superconducting gap displays the temperature evolution, indicating that the gap closes at the critical temperature estimated to be 44.6 and 34.6 K, respectively. According to the aforementioned ADM findings, the results can guide as a characteristic that favors superconductivity. This in turn implies that the ADM and ME methods display a considerable decrease on the $T_c$ from 150 to 200 GPa.

To this end, it is interesting to compare the superconducting properties of Al$_3$Zr$_{0.5}$H$_3$, AlH$_3$, and ZrH$_3$, respectively, as presented in Table 1. First, the qualitative prediction is theoretically confirmed by using first-principle calculation, based on phonon-mediated superconductivity. Note that Al$_3$Zr$_{0.5}$H$_3$ is found to be significantly higher in $T_c$ than AlH$_3$ and ZrH$_3$ at the pressure of 100 GPa. Second, especially, the $T_c$ qualitative prediction is quantitatively revealed by first-principle calculations with Migdal–Eliashberg theory. At the pressure of 100 GPa, there are noticeable increases in $T_c$.

Figure 5. Anisotropic superconducting gap $\Delta$ as a function of temperature at pressures of 100, 150, and 200 GPa; the dot line represents superconducting gap $\Delta$ values, estimated using the isotropic Migdal–Eliashberg formalism.
weakened by the magnitude of electron anharmonicity effect because the acoustic phonon mode is a function of temperature at a pressure of 100 GPa; the dotted line represents the experimental observation of superconductivity should be expected by synthesizing the $A_{0.5}Zr_{0.5}H_3$ structure. Finally, we point out that the existence of unexpected good symmetry can pave the way for further studies and research on the development of high-temperature superconductors.

## AUTHOR INFORMATION

**Corresponding Author**

Thiti Bovornratanaraks — Extreme Condition Physics
Research Laboratory and Center of Excellence in Physics of Energy Materials (CE:PEM), Department of Physics, Faculty of Science, Chulalongkorn University, Bangkok 10330, Thailand; Thailand Center of Excellence in Physics, Ministry of Higher Education, Science, Research and Innovation, Bangkok 10400, Thailand; orcid.org/0000-0001-6943-4032; Email: thiti.b@chula.ac.th

**Authors**

Pruttipong Tsuppayakorn-aek — Extreme Condition Physics Research Laboratory and Center of Excellence in Physics of Energy Materials (CE:PEM), Department of Physics, Faculty of Science, Chulalongkorn University, Bangkok 10330, Thailand; Thailand Center of Excellence in Physics, Ministry of Higher Education, Science, Research and Innovation, Bangkok 10400, Thailand

Rajeev Ahuja — Materials Theory, Department of Physics and Astronomy, Uppsala University, SE-751 21 Uppsala, Sweden; Department of Physics, Indian Institute of Technology (IIT) Ropar, Rupnagar 140001 Punjab, India; orcid.org/0000-0003-1231-9994

Wei Luo — Materials Theory, Department of Physics and Astronomy, Uppsala University, SE-751 21 Uppsala, Sweden

Complete contact information is available at:
https://pubs.acs.org/10.1021/acsomega.2c02447

**Notes**

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