Who Authored *On Liberty*? Stylometric Evidence on Harriet Taylor Mill’s Contribution

Christoph Schmidt-Petri, Michael Schefczyk and Lilly Osburg

Department of Philosophy, Karlsruhe Institute of Technology, Karlsruhe, Germany
E-mail: Christoph.Schmidt-Petri@Kit.Edu

Abstract
It is well known that John Stuart Mill (JSM) repeatedly acknowledges Harriet Taylor Mill’s (HTM) substantial contribution to *On Liberty*. After her death, however, he decides to publish the book under his name only. Are we justified in continuing this practice, initiated by JSM, of refusing unequivocal co-authorship status to HTM? Drawing on stylometric analyses, we make a preliminary case that JSM did not write *On Liberty* all by himself and that HTM had a hand in formulating it. Drawing on plausible standards for authorship ascription, we further point out that authorship status requires, in addition to a substantial contribution, the approval by all contributors. We discuss potential reasons to assume that HTM did not approve the published version of *On Liberty* and would have objected to including her name on the title page.

1. Introduction
The authorship of *On Liberty* has been a cause of puzzlement since its first publication in 1859. In the famous dedication, John Stuart Mill declares that his deceased wife Harriet Taylor Mill ‘was the inspirer, and in part the author, of all that is best in my writings […]. Like all that I have written for many years, it *[On Liberty]* belongs as much to her as to me.’\(^1\) The *Autobiography* adds further details to this picture: ‘After it *[On Liberty]* had been written as usual twice over, we kept it by us, bringing it out from time to time and going through it *de novo*, reading, weighing and criticizing every sentence. Its final revision was to have been a work of the winter of 1858–59 […].’\(^2\) John Stuart Mill presents *On Liberty* as the joint product of two persons who discussed every sentence of the text.\(^3\)

\(^1\)John Stuart Mill, *On Liberty*, CW XVIII, 216. ‘CW volume number, page number’ refers to the *Collected Works of John Stuart Mill*, ed. by John M. Robson and Jack Stillinger (Toronto: University of Toronto Press, London: Routledge and Kegan Paul, 1963–91).
\(^2\)CW I, 249.
\(^3\)See also: ‘The *Liberty* was more directly and literally our joint production than anything else which bears my name, for there was no sentence of it that was not several times gone through by us together, turned over in many ways, and carefully weeded of any faults, either in thought or expression, that we detected in it’ (CW I, 258–59).

© The Author(s), 2021. Published by Cambridge University Press. This is an Open Access article, distributed under the terms of the Creative Commons Attribution licence (http://creativecommons.org/licenses/by/4.0/), which permits unrestricted re-use, distribution and reproduction, provided the original article is properly cited.
So why did he decide to publish the book under his name only? Whatever his reasons might have been, do we have good reason to continue this practice of denying unequivocal co-authorship status to Harriet Taylor Mill? We call this normative question the *On Liberty Authorship Puzzle*. The issue is no trifle. *On Liberty* is part of the philosophical canon. If Harriet Taylor Mill (hereafter HTM) should be credited as author next to John Stuart Mill (hereafter JSM), it would be the first time that a central text in the history of political philosophy would change authors after its publication.

The still prevalent answer to the authorship puzzle consists in (i) contesting that HTM’s contribution was in fact as significant as JSM asserts and (ii) claiming that this justified JSM’s decision to deny HTM unequivocal co-authorship status. We call this the *conservative solution* to the authorship puzzle. The evidence currently available does not contradict the conservative solution: apart from JSM’s sweeping assertions, we do not have any detailed record about who is responsible for particular ideas or specific formulations in *On Liberty*. Furthermore, concerning the intellectual capacities of his wife, the reliability of JSM’s testimony was already questioned by Mill’s contemporaries. His friend and biographer Alexander Bain even refers to Mill’s assessment of her capacities as ‘hallucinations.’

The extent and nature of her contribution has ever since been cast into doubt. The first to demur regarding the conservative solution was Hayek. If JSM is generally considered to be a highly reliable source, what reason is there to doubt his testimony on HTM specifically? Hayek himself reserves judgment on HTM’s capacities but clashes with the conservative solution in confirming her strong influence on JSM’s thinking. Since the 1970s scholars have increasingly challenged the conservative solution as the product of essentially sexist assumptions in combination with an inappropriate understanding of how authorship should be conceptualised. These scholars give support to

---

4. Cf. Rossi: ‘It remains a puzzle why, if her contribution [to *On Liberty*] was so great, everything appeared under Mill’s name alone’, in *Sentiment and Intellect: The Story of John Stuart Mill and Harriet Taylor Mill*, in *Essays on Sex Equality: John Stuart Mill and Harriet Taylor Mill*, ed. by Alice Rossi (Chicago: University of Chicago Press, 1970), 39.

5. Alexander Bain, *John Stuart Mill: A Criticism with Personal Recollections* (London: Longmans, Green & Co., 1882), 171; S. E. Henshaw, John Stuart Mill and Mrs. Taylor, *Overland Monthly*, 13 (1874), 523; William Courtney, *The Life of John Stuart Mill* (London: Walter Scott, 1889), 119; Guy Linton Diffenbaugh, Mrs. Taylor Seen Through Other Eyes Than Mill’s, *Sewanee Review*, 31 (1923), 202–04; Ruth Borchard, Mill: The Man and the Thinker, *The Contemporary Review*, 185 (1954), 103; H. O. Pappé, The Mills and Harriet Taylor, *Political Science*, 8.1 (1956), 27f.

6. F. A. Hayek, *John Stuart Mill and Harriet Taylor: Their Friendship and Subsequent Marriage* (London: Routledge and Kegan Paul, 1951), 15.

7. Hayek, *Friendship*, 17.

8. Rossi, *Essays*; Susan Gorag Bell, The Feminization of John Stuart Mill, in *Revealing Lives*, ed. by Susan Gorag Bell and Marilyn Yalom (Albany: SUNY Press, 1990), 81–92; Virginia Allen, On Liberty and Logic, In: *Listening to Their Voices*, ed. by Molly Wertheimer (Columbia: University of South Carolina Press, 1997), 42–68; Jo Ellen Jacobs, The Lot of the Gifted Ladies is Hard, in *Hypatia* 9 (1994), 132–64, and Harriet Taylor Mill’s Collaboration with John Stuart Mill, in *Presenting Women Philosophers*, ed. by Cécile Tougas and Sara Ebenreick (Philadelphia: Temple University Press, 2000), 155–66; and: The *Voice of Harriet Taylor Mill* (Bloomington: Indiana University Press, 2002); E. Forget, John Stuart Mill, Harriet Taylor and French Social Theory, in *The Status of Women in Classical Economic Thought*, ed. by Robert Dimand and Chris Nyland (Aldershot: Elgar, 2003), 285–310; Mariana Szapuová, Women in Philosophy: The Case of Harriet Taylor Mill, in *Human Affairs*, 2 (2006), 133–43; Meneka Philips, The ‘Beloved and Deplored’ Memory of Harriet Taylor Mill, in *Hypatia*, 33 (2018), 626–42. Gertrude Himmelfarb’s position is hard to locate. According to her, the ‘whole mode of thinking’ in *Liberty* is
what may be called the critical solution to the authorship puzzle: (i) HTM’s contribution was at least as significant as JSM asserts, and (ii) he should not have denied her authorship. The critical solution presses us to reconsider our understanding of the ways a bona fide author has to contribute to a text (other types of input than writing should count as contribution), but it also confronts us with a troubling conclusion regarding JSM. Does he, still the most notable male feminist in the history of philosophy, play a part in the problematic practice of ‘downgrading, making invisible, and concealing the position of women in the field of philosophy’? We call this the downgrading charge against Mill.

The critical solution also has its problems, though. It is mainly grounded in JSM’s testimony, which unfortunately is not unambiguous. Dale Miller reminds us that JSM does not mention HTM as co-author of On Liberty in his personal bibliography, and in letters ‘he refers to the essay as his and to himself as the one writing it’. On 5 October 1857 JSM writes to Theodor Gomperz: ‘I have nearly finished an Essay on “Liberty” which I hope to publish next winter.’ And on 4 December 1858 he lets Gomperz know that he lost Harriet, his ‘perfect friend, companion, guide, teacher’ and that his ‘small volume on Liberty will be published early this winter’, without addressing issues of joint authorship. To HTM he writes on 15 January 1855 that he ‘came back to an idea we have talked about, & thought that the best thing to write & publish at present would be a volume on Liberty’. If Harriet agrees ‘I will try to write & publish it in 1856 if my health permits as I hope it will.’ These letters and the bibliography seem to suggest that Mill was truly convinced that he is the sole author of On Liberty, and indicate that his sole authorship may always have been the Mills’ joint plan. Even though we agree with Jacobs’ heuristic for authorship attribution, namely that ‘Without substantial evidence to the contrary, it seems reasonable to believe that work is collaborative if participants say it is’, it unfortunately is not entirely clear what the participants do say in this case.

After more than 150 years of debate the picture is therefore still inconclusive. In this article, we present a new approach which promises progress on two fronts. The largest part of our work consists in applying stylometric methods to On Liberty. Briefly, stylometry extracts the writing style of a person from his or her texts and then compares this ‘stylome’ to the stylome of texts the author of which is yet to be identified. Stylometric analyses depend on a number of potentially controversial premises, as explained in greater detail below. According to the models we present, one can say with some degree of confidence that JSM did not write On Liberty all by himself and that HTM played a part in putting parts of the text into words. Even though we do

---

1‘difficult to reconcile with Mill’s other works.’ If one had to decide for a single person to whom it belongs, it would be HTM. Himmelfarb is certain ‘that it was she who provided the ‘single truth’ which forms the center of the book, cf. On Liberty and Liberalism (New York: Knopf, 1974), 259f.

2Mariana Szapuová, Women, 133; Ruth Edith Hagengruber, The Stolen History, in: Methodological Reflections on Women’s Contribution and Influence in the History of Philosophy, ed. by Ruth Edith Hagengruber and Sigridur Thorgeirsdotir (Cham: Springer, 2020), 43–64.

3Dale E. Miller, Harriet Taylor Mill, in The Stanford Encyclopedia of Philosophy (Spring 2019 Edition), ed. by Edward N. Zalta, https://plato.stanford.edu/archives/spr2019/entries/harriet-mill/.

4CW XV, 539.

5CW XV, 581.

6Hayek, Friendship, 17.

7Ibid.

8Jacobs, Collaboration, 157.
not have available the gold standard evidence for *On Liberty*, such as pencil marks and handwritten comments, which Stillinger could use in his 'Who wrote J. S. Mill’s *Autobiography*?' The statistical models on which our stylometric ascriptions are based are decidedly better than intelligent guesses. By exploiting this hitherto unused source of information, we hope to put a gridlocked debate in motion. Although we consider our results as preliminary, we are convinced that stylometric methods have the potential to bring us closer to a satisfying solution of the authorship puzzle.

In addition to this new kind of empirical evidence, we offer considerations on conditions for authorship attribution, an issue that has remained underdeveloped in the debate so far. We will draw on relatively uncontroversial principles for authorship ascription found in guidelines for good scientific practice. Notwithstanding the stylometric case for HTM’s contribution we present, there might have been normatively acceptable reasons for JSM to publish the book under his name only. In that sense, both the conservative and the critical solution would be mistaken.

We proceed as follows. In the second section, we describe the periods of cooperation between JSM and HTM, outline our position on attribution of authorship and sketch the objective and scope of our analysis. Sections 3–5 present the evidence on HTM’s contribution: the third section describes stylometry and how it helps to distinguish who of several potential ‘scribes’ has actually written a passage. In the fourth section, we present the first results of our project with a simple cluster analysis on our entire corpus. The fifth section presents the second set of results, using the ‘rolling classify’ function of the software package *Stylo*, which detects the most likely author of specific sections of *On Liberty*. The sixth section reconsiders the authorship puzzle against the backdrop of our results and argues that the downgrading charge against JSM might well be mistaken.

2. Cooperation and authorship

Because our stylometric methods compare *On Liberty* with other paradigmatic texts of the potential authors, it is of crucial importance first to understand clearly which texts would be suitable candidates for comparison.

Ideal conditions for stylometric analyses are the following: (i) *Same genre*: The stylome is influenced by the genre; thus, one gets better results if one compares texts that belong to the same genre. (ii) *Same period*: The stylome might change over time; thus, it is better to compare texts from the same period. (iii) *Enough text*: The more text of any author there is, the more accurately the stylome may be extracted. (iv) *Same amount of text*: If there is much more text of one author than of the other, the models might get biased; thus, it is better to have a similar amount of texts from all potential authors.

---

16 Jack Stillinger, Who wrote J. S. Mill’s *Autobiography*?, *Victorian Studies*, 27.1 (1983), 7–23.

17 Ronald Bodkin claims that ‘by the rules of current scholarship, an excellent case can be made that Harriet Taylor should have been listed as a co-author of the *Principles*,’ see Women’s Agency in Classical Economic Thought, *Feminist Economics*, 5.1 (1999), 45–60, at p. 48.

18 We use ‘scribe’ neutrally to denote someone who produces an inscription, the writing down of thoughts in natural language. Discussing Loesberg, Jacobs rejects the view that one can conclude from a person’s ‘not being a scribe’ that said person is not a co-author. We agree. Being a scribe is neither necessary nor sufficient for co-authorship, but a prima facie-reason to assume that that person is a (co-)author, cf. Jacobs, *Collaboration*, 156.

19 An appendix elaborating on some technical matters is available on the *Utilitas* website.

20 For details, see the appendix.
(v) Correct labels: The texts one uses in order to build the stylometric model must be correctly labelled initially.

Conditions are less than ideal in all respects when it comes to the cooperation of JSM and HTM. The authorship of many texts in the relevant corpus is controversial, the corpus of HTM is very thin in comparison to JSM’s, and one cannot exclude the possibility that the analyses are affected by genre and period effects. For instance, it is plausible to believe that before the first meeting of JSM and HTM in 1830 and after HTM’s death in 1858, their respective individual writing styles would have been different from their styles during their phase of cooperation. Even though including texts from these periods would in principle allow for a more precise stylistic analysis due to the larger quantity of text, this potential change in style would provide a source of error. We therefore restrict our analysis to the phase from 1831 to 1858.

In the years 1831 till 1849, the year of the death of HTM’s first husband John Taylor, we see a very productive period for HTM, a large number of newspaper articles co-written by HTM and JSM, and two major books published under JSM’s name: the System of Logic in 1843 and the Principles of Political Economy in 1848. The next phase lasts from 1850, the year of their marriage, till 1858, the death of HTM. There are few texts published under JSM’s name in this phase (the main texts being ‘Whewell on Moral Philosophy’ and the reviews of Grote’s History of Greece). The fourth phase, the years till 1873, the year of JSM’s death, sees the publication of many of his most famous pieces. Of particular interest here are On Liberty (1859), Utilitarianism and Considerations on Representative Government (both 1861), Subjection of Women (1869) and the posthumous Autobiography (1873).

The articles published under both names provide the evidence for paradigmatic texts of co-authorship of HTM and JSM. These are mostly newspaper articles. This is somewhat unfortunate because of a presumed genre effect. Newspaper articles differ from academic writings, hence newspaper articles do not represent the best conceivable evidence on a potential joint writing style to be found in the more academic On Liberty. But they are (almost) all we have available.

Of course, we do not take all title pages at face value to assign authorship in our corpus. In some cases, we already have strong evidence that the title page does not reflect actual authorship. The Principles of Political Economy provide a case in point. On some interpretations, all of the chapter entitled ‘On the Probable Futurity of the Labouring Classes’ is assigned to HTM. However, as highlighted by Miller, JSM states clearly that, though HTM might have inspired him to write it, he actually wrote it:

In the first draft of the book, that chapter did not exist. She pointed out the need of such a chapter, and the extreme imperfection of the book without it: she was the cause of my writing it; and the more general part of the chapter, the statement and discussion of the two opposite theories respecting the proper condition of the labouring classes, was wholly an exposition of her thoughts, often in words taken from her own lips.

---

21Most prominently by Jo Ellen Jacobs in The Complete Works of Harriet Taylor Mill (Bloomington: University of Indiana Press, 1998).

22Autobiography, CW I, 255, cf. Miller, Harriet Taylor Mill. The ‘more general part’ and the ‘discussion of the two opposite theories’ mentioned in the quote make up roughly 35% of the chapter. This is where the text ‘often taken from her own lips’ is said to be hidden. Even if we interpret ‘often’ to mean 90%, it would be implausible to claim that the entire chapter was written by HTM.
The authorship of the rest of the Principles is also somewhat controversial. Though it might seem natural to assign all of it to JSM – again, as Miller highlights, though Mill does mention the Principles as co-authored in his Bibliography (‘joint production with my wife’\textsuperscript{23}) the private dedications inserted into some copies given to friends do not mention a co-authorship of HTM at all – we decided to follow the interpretation of Jacobs throughout. That is, we divide the Principles into two parts and attribute Chapter 7 of Book IV to HTM and the rest to HTM and JSM jointly. Though this assignment can certainly be challenged, it is only one of a number of choices we had to make, especially on technical issues, which all might be considered more or less disputable. Instead of trying always to find the ‘best’ solution to each of these issues – a certainly worthwhile and challenging endeavour, but somewhat outside our area of expertise – we considered it more viable to present one well worked-out perspective on the joint production of JSM and HTM, that of Jacobs, as a starting point.\textsuperscript{24} It remains to be seen in the future whether other perspectives will yield better results.\textsuperscript{25}

For instance, starting from a different perspective than Jacobs, it could be argued that we should include even more texts as co-authored by HTM\&JSM in our corpus. After all, JSM himself claims that in a ‘wide sense’, literally all texts written in the period 1831–58 were the ‘joint product of both’, even when the title page says differently. He justifies this claim with a perfect ‘unity of mind’ between the two. According to him, he discussed with HTM ‘all subjects of intellectual or moral interest […] in daily life.’\textsuperscript{26} Would perfect unity of mind be sufficient to count HTM as co-author of all works written in this period, including On Liberty?\textsuperscript{27} We think this would be a little bit too radical. This approach would go much further than even what the adherents of the critical solution endorse, who emphasise that HTM made a genuine yet somewhat hidden contribution to many texts. They claim that HTM did not merely agree with everything JSM said or wrote – perfect unity of mind would not entail more than that – but, in addition, has had a detectable impact on what JSM said or published under his name.

Contemporary research integrity guidelines reflect this plausible view, common ground in the debate, that a substantial and identifiable contribution to a text is required for authorship. Individuals who did not contribute to a publication must not be listed as co-authors. This is intended to exclude so-called guest/gift/honorific and (of course)
forged authorship. The contribution required by this contribution condition, as we call it, may consist in different things, such as taking part in the conception or design of a work, drafting or substantially revising it, but merely agreeing with a text is not enough. Hence unity of mind alone would not be a contribution in the required sense, and HTM should not be counted as co-author of On Liberty on this basis.

In many cases, however, Mill maintains that HTM did contribute to the production of specific texts. Unfortunately, neither JSM nor HTM identified how she did contribute with sufficient precision. As mentioned above, the conservative solution doubts that HTM’s part was substantial enough to satisfy the contribution condition. It is controversial whether less tangible contributions such as the verbal provision of ideas, feedback on text or thoughts, background knowledge or a general outlook would at all satisfy this condition, but it should not be controversial that the writing of actual text does satisfy it. If one can identify such traces of an individual scribe, one normally has strong evidence for assuming that the contribution condition is met by this individual. This is what we are attempting to achieve.

A second fundamental principle of authorship attribution in collaborative work may be called the approval condition. The approval condition is normative. It emphasises that authorship entails co-responsibility for the content of the publication as a whole. In a joint publication, each author can be held accountable for the contributions of other authors. Thus, each author must know, understand and approve – to a degree deemed sufficient by the co-authors – what is being published in his or her name. Anyone listed as co-author is within reasonable bounds answerable for the content of the publication as a whole. Certainly, each person mentioned as author should explicitly approve of the final version and could veto being listed as author.

Jacobs applies something like the approval condition with regard to ‘Enfranchisement of Women’. She claims JSM assigned authorship to HTM although they ‘clearly worked together on drafts of ideas that would serve as the core of the article’. According to Jacobs, the reason was that the ‘article contained ideas with which John did not completely agree’. We similarly believe that, in the case of On Liberty, we have to take seriously the possibility that it was HTM who did satisfy the contribution condition, but not the approval condition.

28Marcia K. McNutt and others, Transparency in Authors’ Contributions and Responsibilities to Promote Integrity in Scientific Publication, Proceedings of the National Academy of Sciences 15.11 (2018), 2557–60, on p. 2558.
29It has been argued that providing input when refereeing might in certain cases already satisfy it, see Thomas C. Erren, Michael Erren and David M. Shaw, Peer Reviewers Can Meet Journals’ Criteria for Authorship, British Medical Journal, 2013;346:f166.
30For an informed discussion of various kinds of typical contributions, see Harold Love, Attributing Authorship (Cambridge: Cambridge University Press, 2002), ch. 3.
31Note that an individual might also fulfil the contribution condition and merit being mentioned as co-author without leaving detectable traces. If one detects signals of HTM’s style in On Liberty, this is strong evidence that she contributed written text. But she might still deserve to be considered a co-author even if such a signal may not be found.
32JSM seems to suggest at one point that he generally ‘held the pen’, in other words, that he was the scribe in all or almost all cases. We know from manuscripts that this is not literally true, that HTM was sometimes even holding the pen in writing his Autobiography. Stillinger describes it as palimpsest which may justly be called ‘the Mills’ Autobiography’, Stillinger, Who Wrote, 21.
33Jacobs, The Voice, 218.
3. Stylometry

Our present aim is to determine how much of *On Liberty* has been written by one of the three scribes (JSM, HTM, HTM&JSM). The general strategy is first to detect a particular style for each by analysing texts clearly attributable to them, leaving *On Liberty* out of the analysis. Once this is done, we test which of the three is the most plausible author of *On Liberty*. Later on, we will also determine which sections are likely to have been written by which scribe.

The discipline of stylometry investigates the personal style of an author by applying statistical analyses to his or her texts. The major empirical insight of stylometry, which we take as given, is that authors have specific writing styles, called ‘stylomes’ which, maybe surprisingly, are identifiable by the personal frequency of so-called ‘function words’ such as ‘and’, ‘or’, ‘the’, ‘an’ etc. There is, in other words, a frequency distribution over function words that is characteristic of a particular author (at a particular time, for a particular genre, etc.). Though it may be possible for trained readers to detect very characteristic phrases of specific authors and thus to detect whether, say, it was Kant rather than Wittgenstein who wrote a particular text just by looking at the syntactical information, without even processing the semantics, it has been shown that this traditional ‘close-reading’ technique is much less reliable than modern stylometric techniques. In so-called ‘distant-reading’, computers, not humans, are doing the ‘reading’. They are able to syntactically analyse within seconds a large number of texts, indeed entire corpora of works, and hence can reveal complex patterns human readers with limited cognitive and temporal capacities could not possibly pick up. Computers process texts faster and are (at least in some regards) less biased than humans.

The stylome of an author thus extracted is not normally of independent interest, as it fundamentally only consists of a long list of ‘most frequent words’ (MFWs) in regular use. But, as with *On Liberty*, it is often of considerable interest to determine whether a particular person has actually authored a piece of writing attributed (or not) to him or her. The stylome, if reliably established, may contribute to this. Famous examples of results of such authorship attribution include the long-standing question of what Shakespeare wrote and the recent case of J. K. Rowling, the author of the Harry Potter novels, who turned out to be the author of some crime novels using the pseudonym ‘Robert Galbraith’.

---

34The reasons for this fact are not well understood, however. It often matters how many words are used, and the higher the number, the less important function words become. J. F. Burrows, Word Patterns and Story Shapes, *Literary and Linguistic Computing*, 2 (1987), 61–70.

35Efstathios Stamatakis, A Survey of Modern Authorship Attribution Methods, *Journal of the American Society for Information Science and Technology*, 60.3 (2009), 538–56; Patrick Juola, Authorship Attribution, *Foundation and Trends in Information Retrieval*, 1.3 (2006), 233–334.

36Recently popularised by Franco Moretti in his *Graphs, Maps, Trees* (London: Verso, 2005) and *Distant Reading* (London: Verso, 2013).

37The MFWs may also be character n-grams, a specific sequence of n letters: the 3-gram ‘the’ is a word on its own, but also occurs in ‘theatre’.

38It is helpful to think of the stylome as a photography of a person rather than his or her fingerprint. A picture taken some years later might be an equally reliable representation at that moment, but look very differently, whereas the fingerprint does not change. This analogy might overstate, however, how much the stylome of an author typically changes.

39See Petr Plecháč, Relative Contributions of Shakespeare and Fletcher in *Henry VIII*, *Digital Scholarship in the Humanities*, 2020;fqaa032, [https://doi.org/10.1093/llc/fqaa032](https://doi.org/10.1093/llc/fqaa032), and Joseph Rudman, Non-Traditional Authorship Attribution Studies of William Shakespeare’s Canon: Some Caveats, *Journal of Early Modern*...
Without credible ex-post confirmation by the actual author or further strictly historical evidence such as reliable eyewitnesses, manuscripts with identifiable handwriting, unambiguous notebook entries etc. – all of which may be disputed, too – authorship attribution using stylometric techniques provides less than full proof. At the moment, there is no established procedure for determining precisely how conclusive any particular analysis is, as there is no established procedure on how authorship attribution must proceed.\textsuperscript{40} As mentioned, any stylometric investigation also requires a large number of potentially controversial parameter-setting decisions which might have a major impact on the results. All such choices should at least be made explicit and justified, and there are often good reasons to decide one way or the other. It should be noted, however, that results appealing to distant-reading techniques always ought to be considered as one piece in a larger puzzle only. Ideally, they are supplemented by further kinds of evidence, if available. Yet it is also important to realise that there are parts of the puzzle that only stylometry may contribute. Because stylometry provides an entirely novel kind of evidence, it holds the promise of helping to resolve some traditional questions on which no further conventional evidence may be expected to be forthcoming.

4. A cluster analysis of On Liberty with Stylo

For our analysis, we used the open-source library \textit{Stylo}.\textsuperscript{41} \textit{Stylo} is the state-of-the-art analysis tool for stylometry. It is a library for R, a free and well-established programming language for statistical computing for which supplementary packages are developed, serving specific interests. It is continuously being updated and improved by the \textit{Computational Stylistic Group}.\textsuperscript{42} \textit{Stylo} offers several settings when analysing corpora. For our project, so-called ‘cluster analysis’ and ‘rolling classify analysis’ are the two fundamental features.

As a first illustration, consider Figure 1 below, displaying a cluster analysis, which groups texts together by their stylometric distance. Its inputs are individual texts in their entirety, not sections of texts. The texts first need to be prepared and formatted (cf. the online appendix). As described in section 2, of some of these texts, we take the authorship as given, these begin with ‘htm’, ‘jsm’, or ‘htm&jsm’, as the case may be. We do not attribute an author to the text of interest for us, \textit{On Liberty}, hence it begins with ‘test’. \textit{Stylo} then computes the MFWs for each of the texts, and groups the texts together, using a distance measure (without taking into account the file names).\textsuperscript{43} The overall cluster analysis runs on our entire corpus, consisting of 273
texts. It’s impossible to display the entire diagram, so we may only show an illustrative section of a slightly reduced yet representative corpus.44

The main result is that On Liberty clusters most closely with Considerations on Representative Government. This means that there is no text in the entire corpus that is more similar in its stylome to On Liberty than Considerations. The next closest texts are The Subjection of Women and Utilitarianism, and then follows, perhaps surprisingly, ‘Enfranchisement of Women’. Thus, according to the section of the graph visualised, it looks like On Liberty was written by JSM. Furthermore, apparently so was ‘Enfranchisement of Women’, as this text too clusters very closely with other texts by him, rather than closely to texts written by HTM.

We also note that the co-authored newspaper writings closely cluster together. This indicates that the cluster analysis reliably identifies the different authors – those texts which were co-authored (according to the title page) do have a distinct stylome. However, it is impossible to disentangle this signal of co-authorship from a potential genre effect.45

Figure 1. Cluster analysis.

44The entire diagram is available on our website.

45This cluster analysis is based on the cosine delta distance measure, 1500 MFW, culling at 0% (all texts are included in their entirety; we do not remove words which only occur in some texts). Stylo also offers a ‘bootstrap analysis’ as robustness check, displaying the results of a large number of analyses under different settings. Our results are robust.
5. Classify and rolling classify

The cluster analysis clearly suggests that *On Liberty* is more like texts by JSM than those by HTM or HTM&JSM. This provides some evidence that HTM did not substantially contribute to it. However, the cluster analysis treats the entire text as one big heap of words, ignoring any internal structure. If, for instance, HTM had written some paragraphs all by herself, using a very characteristic stylome, but those paragraphs were so short that they made up only a small proportion of the overall text, the cluster analysis would not show this, given that it is designed to show only similarities among texts as a whole. The contribution, even if real, would be so minor in terms of how it changes the word frequencies of the overall text that it could not push the text over to the co-authored items or the texts written by HTM on her own. This is an inherent limitation of cluster analyses, which are not designed to look inside the texts.

For this reason, the second analysis we want to perform is a ‘rolling classify’ analysis. Such an analysis divides a text into overlapping sections of a given size and then computes the most plausible author of each section. A rolling classify analysis thus allows us to detect authorship signals that appear only in certain parts of the text. This is the mechanism most suitable to detect the exact location at which individual scribes have contributed in terms of formulating the text.

Before we get there, however, we need to describe how the classify mechanism works. The ‘mechanism’ actually is a machine learning algorithm which determines the author of any text from a given set of potential authors by testing and refining models predicting authorship. Intuitively, we are trying to find the algorithm most reliable in building a model to detect who authored which text. Once we have determined this, we will use the model to classify the individual sections of *On Liberty*. *Stylo* offers several such algorithms, two widely used ones of which are the support vector machine (SVM) and the nearest-shrunken centroid (NSC). We decided to use both so as to be able to compare their results.

Finding the most appropriate settings for the models tested by the algorithms was the most challenging aspect of this project, as there are many interacting problems to address, each of which generates a huge amount of data. The settings are of crucial importance as they radically change the results. Abstractly speaking, this process, called ‘cross-validation’, consists of two steps, training and testing. The training works as follows. We are assuming we know the authorship of all texts, except *On Liberty*, which we remove from the corpus entirely. We are now ‘training’ the models using the algorithms to reliably detect who authored which of all the other texts. For this, 10% (or 20%) of the texts of each author are removed from the corpus. These are the ‘test set’; the remaining texts constitute the ‘training set’. The algorithms then use a ‘black box’ deep-learning mechanism on the training set to improve how well the models detect the respective authors. This training procedure gets repeated 100 times, with random divisions of test and training set.

The resulting models are then checked for their quality using the test set. This cross-validation serves to test the ‘accuracy’ of the model. If a particular setting of the model used by a particular algorithm yields a model with 70% accuracy, for

---

46 Maciej Eder, Rolling Stylometry, *Digital Scholarship in the Humanities*, 31.3 (2016), 457–69.
47 Matthew L. Jockers and Daniela M. Witten investigate the comparative performance of these algorithms: A Comparative Study of Machine Learning Methods for Authorship Attribution, *Literary and Linguistic Computing*, 25.2 (2010), 215–23.
instance, that means 70% of the texts in the test set have been identified correctly by that model.\(^{48}\)

Clearly, such a procedure raises a number of issues. We don’t understand intuitively how the models identify scribes. Even if we understand the underlying theoretical idea, we may only see how accurately they do so. This inherent limitation of machine learning might be intellectually disappointing. More problematically, the accuracy in this sense does not seem to be a valid criterion to decide between models. For example, if a 70% accuracy on average is derived from a 95% accuracy for JSM, but only a 50% accuracy for HTM (i.e. not better than chance) and an accuracy of 75% for HTM&JSM, this is of little help for determining the potential contribution of HTM. In fact, we have reason to believe this exact problem could arise in our case, as the corpus for JSM is much larger than are the corpora for HTM and HTM&JSM. Because of this, unclear cases are more likely to be correctly classified as JSM even by a chance process, because the vast majority of texts will actually be his. This is the so-called ‘class imbalance’ problem. Training the algorithm on an imbalanced set so as to achieve high accuracy does not help us addressing our research question.

The machine learning literature provides different approaches to this problem. We chose to follow the procedure described by Efstathios Stamatos (details are to be found in the online appendix).\(^{49}\) We are going beyond this approach in one important way, however, because we are not focusing on accuracy alone, but also consider ‘precision’ and ‘recall’.\(^{50}\) We have inserted the relevant numbers in six confusion matrices (see Figure 2).

A confusion matrix displays how well any particular model works, for a particular set of parameters. Most applications are binary classifications, and in such a case, a confusion matrix would contain four cells only. For instance, if some texts should be assigned to author A or author B, who are known to be the only two possible authors, there are four logically possible outcomes – two true and two false cells. In our case, the confusion matrices have nine cells. They show how many of the texts actually written by JSM (in the respective second lines, the true label is ‘jsm’) the model correctly identifies or ‘predicts’ as written by him (second line and second column, the predicted label is also ‘jsm’), incorrectly as not having been written by him (second line and first or third column), and, of those actually not written by him (but by HTM, first line, or HTM&JSM, third line), as correctly written by HTM or HTM&JSM, as the case may be, or, incorrectly, as written by him.\(^{51}\)

\(^{48}\)Accuracy is the number of correctly identified cases divided by the total number of cases: for ‘TP’ meaning ‘true positive’ and ‘FN’ meaning ‘false negatives’, etc., accuracy is defined as: TP+TN/(TP + FP + FN + TN).

\(^{49}\)Efstathios Stamatos, Author Identification: Using Text Sampling to Handle the Class Imbalance Problem, Information Processing and Management 44 (2008), 790–99.

\(^{50}\)Precision gives the number of correctly identified cases divided by all identified, whether correctly or incorrectly. Precision (or ‘positive predictive value’) is defined as: TP / (TP + FP). Recall gives the number of correctly identified cases divided by the correctly identified ones plus those falsely not identified. Recall (or ‘sensitivity’) is defined as: TP / (TP + FN).

\(^{51}\)For any author, there is one cell with true positives and two cells each with false negatives, true negatives, and false positives. For instance, the value 0.97 for true label = JSM and predicted label = JSM in the very centre of the first confusion matrix means that the model generating this matrix manages to identify 97% of the papers actually written by JSM as written by JSM. Only 0.28% of his papers are attributed to HTM, and 3% to both; there is a rounding error. Accuracy, precision and recall of the respective models are then computed using these figures.
The predictive models with a total number of 8800 settings we tested all differ in the values they yield. At the end, we had to make a decision on which model to use. This decision necessarily involves a trade-off: some models score more highly in some cells, others in others. Because in practice there is no single predictive model that is better than all others in all cells, there is no single ‘right’ solution on which model and which settings to use, and no ‘right’ answer to the question of which of these cells is more important than the others.

The machine learning literature offers a number of common measures giving different weights to the cells and their combination, that is, giving different weights to precision and recall, in order to achieve a sensible compromise. The ideal scenario would of course be a model that has perfect precision and perfect recall, but perfect precision and perfect recall are not achievable in our case.52

We decided to go with what to us appeared the most neutral measure, the so-called ‘F1-measure’, standard in the machine learning literature. It does not simply average

52100% precision would mean that the model does not produce any false positive results – it would not assign texts to HTM that have not been written by HTM. 100% recall would mean that the model does not produce any false negative results – it would assign all texts to HTM that she has actually written and not miss any.
precision and recall, it strikes a balance by measuring their harmonic mean.\textsuperscript{53} Intuitively, the harmonic mean gives less weight to the more extreme values recorded than the arithmetic mean (colloquially known as average). The idea is that both precision and recall are important, and that a very good value for one of the two should only partially compensate a terrible value for the other: We would rather have a model that scores alright on both objectives than one that scores phenomenally well on the one but terribly on the other.\textsuperscript{54} The F1-score is computed for each line and then macro-averaged.\textsuperscript{55}

We optimised the F1 value for several settings for our two algorithms. In the authorship attribution literature, it is common practice to display only one or very few different final results, but we thought that, in order to obtain a complete picture, it would be more helpful to be able to compare several different algorithms. Our reasoning on which settings to use was as follows.

Clearly, we would have to include both SVM and NSC, as these are the most widely used algorithms, and we wanted to see whether their results confirm or contradict each other. Our impression was that SVM is generally deemed more reliable than NSC, so we used four different SVM settings and two different NSC settings. Those settings which yield the best F1 value across the board, for both SVM and NSC, needed to be included.\textsuperscript{56} We also wanted to detect the effect of our sampling procedure and hence included the SVM and NSC settings with the highest F1-score using the sampling. Even though the sampling should control for the class imbalance problem, we were worried that because of the low number of co-authored HTM&JSM pieces and the presumed genre effect, giving equal weight to the line with the co-authored items might distort the overall results. Hence we also included the two best SVM analyses that only consider the lines for JSM and HTM, one without sampling, one with it. These would be somewhat less reliable in detecting joint authorship of course, but more reliable in detecting each of the other authors. The remaining trade-off between HTM and JSM we decided to resolve using the harmonic mean rather than the arithmetic mean, as all algorithms tended to perform significantly better on detecting JSM.

Consider Figure 3. Its six diagrams display the text of On Liberty, and the dotted lines mark the chapters.\textsuperscript{57} The lower half of each diagram displays the most probable author of the relevant section, the upper half the second most probable (HTM is in black, JSM in light grey, HTM&JSM are in dark grey). The longer the lines, the higher the level of certainty of the classification. The two lower diagrams, using the NSC algorithm, look somewhat different from the top four, using the SVM algorithm, but the basic idea is the same.\textsuperscript{58}

\textsuperscript{53}The precise formula for the F1-measure is: $F1 = 2 \times (\text{precision} \times \text{recall}) / (\text{precision} + \text{recall}) = TP / [TP + \frac{1}{2} (FP+FN)]$. Other measures give more weight to either precision or recall.
\textsuperscript{54}As a simple illustration, the arithmetic mean of 1 and 3 is 2, but the harmonic mean is 1.5; the arithmetic mean of 1 and 7 is 4, but the harmonic mean is 1.75.
\textsuperscript{55}‘Macro-averaging’ means that the F1-scores for all three lines are added and then divided by three. The ‘weighted’ F1-score would compensate for the different number of texts in each class. Because we solve the class-imbalance problem using sampling, this appeared redundant to us.
\textsuperscript{56}The settings are described in n. 58.
\textsuperscript{57}The very beginning is a bit blurry because of the dedication.
\textsuperscript{58}From top to bottom, this displays the rolling classify diagrams for the following algorithms and settings (for all, slice size is 5000 and overlap is 4500):

A. The best F1 value for SVM across the board. The parameters that yield this value turn out to be: without sampling, with newspaper articles, a $p$-value of 20, and using 1700 most frequent words (MFWs).
B. The best F1 value for SVM that includes sampling. The parameters that yield this value turn out to be: with newspaper articles, a p-value of 10, k-value of 95 and MFW at 4700.

Figure 3. Rolling Classify Analyses A–F (for settings, see footnote 58).
6. Results and implications for the authorship puzzle

Let’s first note the remarkable result that HTM is the most probable scribe of some sections of *On Liberty* on all analyses. In other words, it is more likely that HTM has written these passages than that JSM has written them (given our corpus and further assumptions). In fact, all analyses converge in judging that HTM and not JSM most probably wrote some parts of chapter 3. This signal is rather weak on diagram B, but very strong on all others. In the top three diagrams, we also see a clear signal of co-writing in chapter 5, and co-writing is indeed most probable for almost all of chapter 5 on diagram B. Two diagrams (A and C) also give HTM&JSM as second-most likely author of large parts of chapter 3 when HTM is the most likely author. For JSM, the clearest result is his exclusive authorship of chapter 2. Chapter 1 is not as clear, as diagrams B and F assign it to HTM, and even in diagrams A, C, and D he is only a little bit more likely to be the author than HTM.

In assessing these diagrams, we should also take into account the values in the corresponding confusion matrices. The first matrix shows that the best setting of the SVM algorithm is very good at detecting JSM, but not nearly as good at detecting HTM. However, it also shows that almost all of the texts actually written by HTM and not assigned to her are assigned to JSM, rather than to both. So in diagram A, this model implies that some of the sections assigned to JSM have probably been written by HTM. The same is true for diagrams B and C, and, to a somewhat lesser extent, diagram F. In the first diagram, JSM also gets almost 30% of the texts written by both of them assigned to him. So, in diagram A, the contribution of JSM to *On Liberty* is probably overestimated. Similarly in diagrams B and D.

In other words: our models generally are very good indeed at detecting JSM, but not quite as good at detecting HTM or HTM&JSM. Thus we can say with a high degree of confidence which parts have not been written by JSM but by the other potential scribes, HTM or HTM&JSM, though it is harder to say which one of the two it was. As both involve HTM, however, we can say with a high degree of confidence that a lot of *On Liberty* has not been written by JSM alone. This is the main result of our stylometric analysis.\(^{59}\)

So what is the upshot for the authorship puzzle? Since its beginning in the nineteenth century, one feature of the debate has been its strong focus on the credibility

---

C. The best F1 value for SVM only considering the lines for HTM and JSM (the joint pieces are not taken into account in computing the F1 value), and taking their harmonic mean. The parameters that yield this value are: no sampling, with newspaper articles, a \(p\)-value of 10, and MFW at 1700.

D. The best F1 value for SVM only considering the lines for HTM and JSM (the joint pieces are not taken into account in computing the F1 value), and taking their harmonic mean, but with sampling. The parameters that yield the best results are: with newspaper articles, a \(p\)-value of 10, \(k\)-value of 60, and MFW at 2000.

E. The best F1 value for NSC across the board. The parameters that yield the best results are: no sampling, with newspaper articles, \(p\)-value of 10, and MFW at 5000.

F. The best F1 value for NSC that includes sampling. The parameters that yield the best results are: with newspaper articles, \(p\)-value of 20, \(k\)-value of 95, and MFW at 5000.

\(^{59}\)Unfortunately, we do not know how much of HTM and JSM, respectively, is contained in HTM&JSM. The more JSM it contains, the less HTM would have contributed to *On Liberty*. 
of JSM’s statements. The ‘evidence’ presented by the sceptics regarding HTM’s role consisted mainly in derogatory assessments of her as a person and thinker; frequently this assessment bordered on the defamatory. However, if our analysis approaches the truth, Mill’s remark that ‘it is of little consequence in respect to the question of originality which of two persons [who have their thoughts and speculations completely in common] holds the pen’ should not be read as implying that HTM had no hand in formulating On Liberty. She was most likely deeply involved in putting central sections of On Liberty into words. According to our analysis, her part in writing was undoubtedly sufficient to fulfil the contribution condition for co-authorship status. If so, the conservative solution to the authorship puzzle has to be rejected.

Though we consider this to be a heartening finding for the feminist cause, it still leaves JSM fully exposed to the downgrading charge. In The Voice of Harriet Taylor Mill, Jacobs wonders why only JSM’s name appears on the book’s cover. She offers two possible explanations which would partially exonerate Mill. First, ‘a book by J.S. Mill would receive a fairer hearing than one by John and Harriet Mill’, second, JSM may have hesitated ‘to place Harriet’s name on a text he feared would be seen as “infidel book”’. She continues that ‘John may have wanted paternalistically to shield her name from potentially intense criticism.’ If we understand Jacobs correctly, she remains somewhat critical of JSM’s decision: neither of the reasons given were actually sufficiently weighty to justify the absence of HTM’s name on the title page, even though JSM might honestly have thought so.

This might be jumping to conclusions, though. In the second section, we introduced the approval condition of authorship: people must not be named as authors of a publication if they do not approve of being so named. We think that contribution and approval are individually necessary and jointly sufficient for legitimate ascription of authorship. Applying the approval condition to the case at hand, one might wonder whether JSM withheld co-authorship status not because HTM did not contribute, but because she did not approve of On Liberty, exonerating Mill completely.

The approval condition has a cognitive dimension (does a person believe that the claims in a text are acceptable?) as well as a volitional dimension (is a person prepared to advocate the claims in a text in public?). Did HTM fully approve of the content of On Liberty, that is, did she approve cognitively? Let us examine different phases of their cooperation and different hypothetical scenarios. One can state with certainty that HTM did not approve of On Liberty while she was well enough to be convinced that she would partake in the manuscript’s reworking. In his dedication, Mill writes that the book did not have the ‘inestimable advantage of her revision’ and that

60 Jacobs, The Voice, 196ff.
61 Autobiography, CW I, 251.
62 Jacobs, The Voice, 250.
63 Virginia Allen makes a similar point. On the basis of a remark that HTM made in a letter dated 12 May 1848 with regard to the dedication of the Principles of Political Economy, Allen conjectures that JSM might have deferred to HTM’s judgment in not including her name on the title page. Allen suggests that in HTM’s opinion her name would interfere with the reception of the book and thereby diminish its impact. See Allen, Collaboration, 44; Jacobs, Collaboration, 159; Hayek, Friendship, 124.
64 Cognitive approval does not require that one personally agrees with every last detail. In joint work, one acts as a team member committed to pursuing a common goal with others. Thus, a team of co-authors has to make joint decisions and this involves usually some degree of compromise and of deference to the judgment of other team members.
important portions had ‘been reserved for a more careful re-examination’. We thus know that HTM did not approve of the later published text of On Liberty at that time. The same is true, of course, of JSM. Since he, too, was convinced that their final revision would make the text better and since it is a requirement of practical reason to prefer the better to the worse, JSM did not approve the final version at that stage. The interesting issue is the phase after it had become clear that there would be no joint revision of the text.

Let’s consider two scenarios. In the first scenario, HTM expressed a last ‘deathbed wish’ concerning On Liberty. If her wish was to be mentioned on the title page, it seems inconceivable that JSM would have ignored the expressed wish of his dying wife, so we can confidently rule out this possibility. If the deathbed wish was not to be mentioned on the title page, Mill did nothing wrong in any case. This scenario would clear JSM of the downgrading charge and cohere with today’s publication and citation practices.

In the second, less hypothetical, scenario, HTM did not express a deathbed wish regarding On Liberty. Because we know that HTM and JSM were convinced they were able to produce an even better book, we now have to ask whether HTM would have approved of being mentioned as future co-author of an as yet unfinished book which, as shown, did not fully satisfy her standards. This involves the second, volitional, dimension of the approval condition. Should we assume that HTM would have approved of figuring posthumously as an author of On Liberty, given its imperfections?

In order to answer this rather knotty question, further aspects have to be considered. The volitional aspect of the approval condition is grounded in respect for a person’s privacy and liberty: people should have a reasonable degree of control over which of their convictions they want to share with whom and under which circumstances. It is wrong to restrain a person’s right to express their views if they want to see them expressed, but it is also wrong to reveal a person’s views if they don’t want them to be revealed. Because of the volitional aspect, it is conceivable that a contributor fully approves of the content of a text yet does not approve of figuring as its author. Jacobs’s and Allen’s considerations would indicate that JSM thought HTM would not have approved of On Liberty for this reason.

The volitional aspect of the approval condition gives some leeway for providing potentially misleading authorship information. The pro tanto duty to be truthful about the authorship of a publication may plausibly be outweighed by unfavourable circumstances, such as a repressive public or state power. Within certain bounds, we assume that strategic deception of others is permissible in unfree societies. If such justifying conditions cease to prevail, though, the duty to be truthful regarding authorship becomes more binding again.

As a result, even if the considerations noted by Jacobs and Allen might have justified the provision of misleading authorship information in bigoted and sexist Victorian times, today they would give no reason to deny HTM the unequivocal status of being ‘the co-author of this classic’. First, it is very unlikely that On Liberty would receive a less fair hearing today if HTM’s name were to appear on the title page – quite the contrary. Second, On Liberty did not actually make a name for being an ‘infidel book’, and it certainly would not be considered thus today. So even if JSM was pursuing a legitimate objective in protecting the good name of his wife, assuming her

\[65\text{CW XVII, 216.}\]
\[66\text{Jacobs, Collaboration, 251.}\]
disapproval for volitional reasons, today there is no need to maintain this protective attitude – again, quite the contrary, as proponents of the critical solution emphasise: HTM now needs to be protected from an undeservedly unfavourable reputation. The circumstances having changed, JSM’s legitimate concerns now pull in the opposite direction.

7. Conclusion

We have made a stylometric case that Harriet Taylor Mill’s contribution to On Liberty is sufficiently substantial for her to count as co-author. We are not claiming that the evidence is conclusive, as further analyses starting from different assumptions might produce different results. Even though we are not able to say with a high degree of confidence which sections Harriet Taylor Mill wrote herself, we are confident that John Stuart Mill did not write On Liberty all by himself.

We also think there is evidence that John Stuart Mill might have thought his wife would not have approved of being listed as co-author, which would completely exonerate him from the charge of illegitimately downgrading her contribution even if it was as substantial as our evidence suggests. In the interest of historical accuracy and of giving credit where it is due, we suggest modern editions should list Harriet Taylor Mill as well as John Stuart Mill as authors of On Liberty.67

Supplementary material. The supplementary material for this article can be found at https://doi.org/10.1017/S0953820821000339

67For comments which have substantially improved the article we thank two anonymous reviewers, and in particular Dale E. Miller, as well as Jonas Osburg and several audiences at KIT. For research assistance we thank Reja Maria Gauß.

Cite this article: Schmidt-Petri C, Schefczyk M, Osburg L. (2021). Who Authored On Liberty? Stylometric Evidence on Harriet Taylor Mill’s Contribution. Utilitas 1–19. https://doi.org/10.1017/S0953820821000339