Weak-Scale Hidden Sector and Energy Transport in Fireball Models of Gamma-Ray Bursts

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(September 2, 2018)

The annihilation of pairs of very weakly interacting particles in the neighbourhood of gamma-ray sources is introduced here as a plausible mechanism to overcome the baryon load problem. This way we can explain how these very high energy gamma-ray bursts can be powered at the onset of very energetic events like supernovae (collapsars) explosions or coalescences of binary neutron stars. Our approach uses the weak-scale hidden sector models in which the Higgs sector of the standard model is extended to include a gauge singlet that only interacts with the Higgs particle. These particles would be produced either during the implosion of the red supergiant star core or at the aftermath of a neutron star binary merger. The whole energetics and timescales of the relativistic blast wave, the fireball, are reproduced.

The discovery of the afterglow [1] associated with some of the gamma–ray bursts (GRBs) and isotropy of the emitted radiation both support the view that the GRBs occur at cosmological distances with a redshift of the order of one. In this sense, GRBs offer a new observational tool for probing the early universe.

There have been several suggestions concerning the generation mechanisms as well as the distributions of photons in the core of the astrophysical object, i. e., the central engine of the GRBs [3]. Among these, for example, the resonant production of gamma rays during the collision of two neutron stars is one possible mechanism [3]. Pertinent to a typical neutron star, the core region of the progenitor has a characteristic radius of $R_0 \sim 10\text{km}$ with roughly constant temperature $k_B T_0 \sim 50\text{MeV}$ and matter density $\rho_0 \sim 10^{14}\text{g}/\text{cm}^3$. The daily GRBs require a burst duration of $1\text{ms} \leq \tau \leq 0.1\text{s}$ with a total energy release of $\sim 10^{53}\text{erg}$.

Given the extensive parameters of the progenitor and the observed power spectrum, it is known that the gamma photons are trapped in the core region. Then one is to think about other possible agents to transfer the correct amount energy in the given time interval through the baryonic load. One possible alternative is neutrinos [5]; however, the mixing of the flavour neutrinos with the sterile one is strongly suppressed in such matter densities, and thus, the oscillation picture runs into difficulties [5]. Another alternative mechanism would come through the axions; however, the transferred power diminishes if the breaking scale of the Peccei–Quinn symmetry gets higher [5]. In fact, the required axion mass cannot be reproduced in known axion models at all [5].

In this letter we work out a different scenario for transporting the energy outside the GRBs central engine. The basic agent of the process is a CP–even, presumably light, scalar particle, $S$, which has no baryonic charges. Such singlets have been proposed to take into account the nonobservation of the standard model (SM) Higgs particle by increasing its invisible decay rate [7]. For clarity of the discussion, we write down the effective Lagrangian describing the interactions between this SM–singlet and the photons as

$$-L_{\text{int}} \equiv \frac{1}{2} m_s^2 S^2 + \lambda_S S^4 + \lambda_\gamma S^2 A_\mu A^\mu$$

(1)

where $A_\mu$ is the photon, and $m_s$ and $\lambda_S$ designate the mass and the quartic coupling of the singlet, respectively. The original model [9] has an unbroken U(1) symmetry associated to the complex nature of this singlet. However, for the purpose of this work the global phase of the singlet is not important so we take it real. In the framework of the hidden Higgs sector models the couplings above take the form

$$\lambda_S \approx \lambda_0^0 + \kappa^2, \quad \lambda_\gamma \approx \kappa \left(\frac{\alpha_0^0}{\pi}\right)^{1/2} A_\gamma$$

(2)

where $\lambda_0^0$ is the bare quartic coupling of the theory, and $\kappa m_\nu$ stands for $hSS$ coupling [10]. In writing these expressions we neglected invariant masses in a given channel compared to the Higgs boson mass. The vertex factor $A_\gamma$ for $h\gamma\gamma$ coupling is a slowly varying function of $\sqrt{s}$, and it is of the order of one [10]. In all computations below we will parametrize results in terms of $\lambda_S$ and $\lambda_\gamma$ without going back to relations above. However, one keeps in mind that numerically $\lambda_\gamma \sim \mathcal{O}(10^{-4}) \kappa$.

The effective Lagrangian (1) describes a real scalar field interacting with itself and photons. The scattering processes following from this Lagrangian are shown in Fig.1. Here the diagram (a) represents $\gamma\gamma \leftrightarrow SS$ scattering with which the conversion of the photons to singlets in the core of the GRBs burster occurs. Furthermore, conversion of singlets to photons outside (baryon–depleted region of) the GRBs central engine happens with the same process in backward direction. To have a description of the energy transport through the strong baryonic load, it is
FIG. 1. Relevant scattering processes following from the interaction Lagrangian \[ \mathcal{L} \] where the wavy lines represent the photon and dashed lines the singlet. The diagram (a) is responsible for conversion of photons to singlets and vice versa. On the other hand, the diagrams (b) and (c) determine the mean free path of the singlets. Convenient to start with the conversion of the photons to the singlets. The relevant cross section reads as

\[ \sigma(\gamma\gamma \rightarrow SS) = \frac{\lambda^2}{24\pi s} \left( 1 - \frac{4m^2_s}{s} \right)^{1/2} \]  \hspace{1cm} (3)

where \( \sqrt{s} \sim 100\text{MeV} \) is the total invariant mass of the annihilating photons. This process occurs in the core of the progenitor, and the produced singlet pairs move out through the surrounding baryonic loading. Before describing the journey of the singlets in the baryon load, it is convenient to compute the rate of energy conversion from photons to singlets. Denoting the four-momenta of the photons by \( k_1 = (\omega_1, \vec{k}_1) \) and \( k_2 = (\omega_2, \vec{k}_2) \), the total amount of energy converted to singlet pairs per unit time per unit volume reads

\[ Q = \int \frac{d^3\vec{k}_1}{(2\pi)^3} \frac{d^3\vec{k}_2}{(2\pi)^3} n(\omega_1)n(\omega_2)(\omega_1 + \omega_2)v_{\text{rel}}\sigma(\gamma\gamma \rightarrow SS) \]  \hspace{1cm} (4)

where \( n(\omega) \) is the equilibrium Bose population of the photons and \( v_{\text{rel}} = 1 - \frac{\vec{k}_1 \cdot \vec{k}_2}{\omega_1\omega_2} \equiv s/(2\omega_1\omega_2) \) is the relative velocity of the two annihilating photons. After integrating \( Q \) over the volume of the core region, the total luminosity for photon–to–singlet conversion becomes

\[ \mathcal{L}_{\gamma\gamma \rightarrow SS} \approx \lambda^2 \frac{10^{70}}{T_9^5} \left( \frac{R}{R_0} \right)^3 \text{erg} \cdot \text{sec}^{-1} \]  \hspace{1cm} (5)

where \( O(m^2_s/(k_B T)^2) \) terms are neglected in computing \( Q \). This is a good approximation in the burster core where temperature is high enough. Assuming that this will be the luminosity observed on Earth, a comparison with the GRBs standard candle luminosity requires \( \lambda \sim 10^{-8} \). As will be discussed later, \( \lambda \) is a loop–induced quantity in the weak–scale hidden Higgs sector models so that such a small number is naturally expected there. Despite all these, however, what is observed on Earth is \( \mathcal{L}_{SS \rightarrow \gamma\gamma} \), that is, one has to convert the singlets back to photons to simulate the experimental conditions so that these naive bounds on \( \lambda \) may vary.

The singlets, after being pair–produced by photon–photon annihilations in the core region, travel through the strong baryonic load towards the baryon–depleted region outside the GRBs burster. Since there is no interaction with the baryons they do not feel the baryonic load at all, and would move freely along radially out–ward trajectories were it not for their self–interactions. It is clear that the temperature of the host baryon distribution does not effect the distribution and dynamics of the singlets as they can never come to thermal equilibrium with the baryons. In this sense, even if the star is quite cold with a small fraction of MeV temperature in the optically thin region, the singlets themselves can be quite energetic to generate the \( SS \rightarrow \gamma\gamma \) reaction. Namely what singlets take out of the star is the energy accumulated in the gamma photons and this happens
dependent of the temperature and density distribution of the baryons.

The singlet self-interactions are depicted in diagrams (b) and (c) of Fig. 1. Both diagrams are generated by the singlet quartic coupling in the Lagrangian. A close inspection of these diagrams reveal some important properties. The $SS \rightarrow SS$ scattering depicted in Fig. 1(b) preserves the number of singlets, is a contact interaction, and is kinematically operative for $\sqrt{s} \geq 2m_s$. The $SS \rightarrow SSSS$ scattering in Fig. 1(c), on the other hand, doubles the number of singlets, is a long–range interaction with range $\sim m_s^{-1}$, and is kinematically allowed when $\sqrt{s} \geq 4m_s$. The relevant cross sections are estimated to be

$$\sigma (\text{Fig. 1(b)}) = \frac{\lambda_s^2}{16\pi s} \gg \sigma (\text{Fig. 1(c)}) \sim \mathcal{O} \left( \frac{\lambda_s^4}{(2\pi)^4 s} \right) \quad (6)$$

so that cross section for $SS \rightarrow SSSS$ scattering is second order in $\lambda_s$ and receives further phase space suppressions.

The most important quantity describing the motion of the singlets towards the GRBs baryon–depleted region is their mean free path. Having no interactions with the baryons, the singlet mean free path would be infinitely long were it not for the singlet self-interactions depicted in diagrams (b) and (c) of Fig. 1. The total mean free path obeys the relation

$$\ell^{-1} = \ell_{(b)}^{-1} + \ell_{(c)}^{-1} \quad (7)$$

where subscripts refer to the diagrams in Fig. 1. Therefore, the total mean path over which singlets move freely is described by the larger of the individual contributions (for Fig. 1(b) and Fig. 1(c), respectively)

$$\ell_{(b,c)}^{-1} = \int \frac{d^3p}{(2\pi)^3} n(E_i) v_{rel} \left( 1 - \frac{4m_s^2}{s} \right)^{1/2}$$

$$\sigma \quad (8)$$

where $n(E_i)$ is the equilibrium Bose population for the target singlet and $v_{rel} \equiv s/(2E_i)$ is the relative velocity of the incident and target singlets with respective four-momenta $p = (E, \vec{p})$ and $p_i = (E_i, \vec{p}_i)$. Here we take the phase space density of singlets as a Bose distribution ignoring the possibility of free streaming. In any case the resulting mean free path will be a conservative estimate of the actual one.

As Eq. (8) suggests clearly, larger the cross section smaller the corresponding mean free path. Using the expressions for the cross sections in (8) one can make the rough estimate

$$\ell \approx \ell_{(b)} \sim \left( \frac{E}{k_BT_0} \right) \left( \frac{50\text{MeV}}{k_BT_0} \right) \left( \frac{10^{-8}}{\lambda_s} \right)^2 \sim 100\text{km} \quad (9)$$

neglecting the terms $\mathcal{O} (m_s^2/k_BT_0^2)$.

This mean free path results solely from the self-interactions of the singlets, that is, it is the singlets themselves which prevent their further flight. In particular, it is not the baryons that limit their motion so that it does not matter if $\ell$ happens to fall inside or outside the baryon load region; literally, singlets will stand still in a sphere of mean radius $\mathcal{O} (\ell)$ measured from the core of the progenitor. To clarify this point further one recalls, for instance, the neutrino propagation. In that case the mean free path is determined by the neutrino–baryon interactions, and if it is outside the GRBs baryon load region neutrinos get out of the astrophysical source otherwise they are trapped by the baryons and form a thermal neutrino sphere. Therefore, the formation of the singlet sphere follows only from their self-interactions.

Due to their self-interactions in Fig. 1(b) and (c) singlets will form a thermalized cloud of particles whose number and energetics will change with a chain of such scatterings. As mentioned before, the $2 \rightarrow 2$ scattering in Fig. 1(b) preserves the number of singlets and plays an important role in restricting the singlets to have the finite mean free path $\ell$. The $2 \rightarrow 4$ scattering in Fig. 1(c), however, is a long–range interaction and it modifies the number of singlets. Due especially to its long–range nature it is effective everywhere in the singlet sphere, and causes largely separated singlet pairs to annihilate into four new singlets. This interaction, thus, increases the number of singlets and reduces the mean energy per capita. The resulting cloud of singlets will thermalize themselves with their self-interactions with a temperature much lower than the burster core temperature. At any point inside the singlet sphere, there will be singlets coming from every direction which is important in computing the energy accumulation in a given region. If singlets were moving along radially outward trajectories there would be a strong geometrical suppression factor for the energy deposition $[11]$.

As mentioned above, because of $2 \rightarrow 4$ process in Fig. 1(c) total number of singlets increases, and thus, average energy per singlet decreases. Similar to the electromagnetic showers initiated by photons, a straightforward computation of the total number of produced singlets as the mean energy per singlet drops from $E_0$ to a critical energy $E_c$ via the $2 \rightarrow 4$ scattering gives $N = N_0 \left[ 1 + (E_0 - E_c)/E_c \right]$ where $N_0$ is the initial number of singlets given by the number of photons. In the problem at hand, $E_0 \sim k_BT_0$ and $E_c \sim k_BT \sim 2m_s$ where the latter follows from the kinematic blocking of $2 \rightarrow 4$ scatterings. Number of singlets per unit volume can be computed over a sphere of radius $\ell$: $\rho = 3N/(4\pi\ell^4)$. Since the singlet cloud eventually thermalizes it is convenient to use the usual Bose population for the number of singlets per unit volume per unit momentum state with an appropriate scaling to reproduce the singlet density $\rho$:

$$\rho = K \int \frac{d^3p}{(2\pi)^3} n(E) \quad (10)$$
where \( n(E) \) is the Bose population of the singlets at temperature \( T \), and \( K \) is a constant for reproducing \( \rho \).

The next thing one needs for computing the electromagnetic power generated by the singlets is the \( SS \rightarrow \gamma\gamma \) cross section

\[
\sigma(SS \rightarrow \gamma\gamma) = \frac{\lambda^2}{8\pi s} \left( 1 - \frac{4m_s^2}{s} \right)^{-1/2} \quad (11)
\]

to be compared with \( \gamma\gamma \rightarrow SS \) cross section in \([3]\). Then computation of the luminosity proceeds in exact similarity with \([3]\) after replacing the cross section there by \([3]\).

\[
\mathcal{L}_{SS \rightarrow \gamma\gamma} = \left( \frac{R_0}{\ell} \right)^3 \left( \frac{T_0}{T} \right)^3 \mathcal{L}_{\gamma\gamma \rightarrow SS}, \quad (12)
\]

where a factor of \( (T_0/T)^2 \) follows from \( (E_0/E_c)^2 \). \( \mathcal{L}_{SS \rightarrow \gamma\gamma} \) is computed over the volume of singlet sphere. Thus, the larger the mean free path the higher the luminosity suppression factor. However, the higher the initial (core) temperature the higher the luminosity emitted. Since both effects scale with the same power it is clear that no energy is lost in the global process, and the mechanism here suggested is able to effectively carry out the overall energy released in the GRBs central engine as in the context of fireball models. Once the energy is out of the baryon loading, a relativistic blast wave of electron-positron pairs and radiation is formed, i.e., a fireball, which cleans away the burster environment pushing out a rather matter free debris to produce the observed burst when colliding with and external interstellar medium. The no-time-delay feature of this scenario makes it suitable to explain bursts with both rapid rise-time and prompt afterglows as observed in GRB990123. The potential role of this mechanism in triggering GRBs from supermassive star explosions is an issue currently pursued. \([4]\).

To conclude, we have investigated the viability of the hidden Higgs sector models of turning realizable the energy transport in GRBs in the context of fireball scenarios \([2]\). As the discussions in the text show, in such models transport of the energy from the core to outside is quite efficient, and the resulting luminosity agrees with the astronomical observations. The particle physics scenarios with neutrinos and axions are not as efficient as the present model due to the suppression of the neutrino mixing angle and smallness of the axions mass, respectively. In the present model, conversion processes are mediated by the Higgs particle. On the other hand, transport of the energy from the core to outside is done by the singlets having a rather large mean free path compared to neutrinos. In the present scenario singlets are light enough to be pair-produced by the photon annihilations, and such a light singlet does not contradict with the present collider data as it affects the precision observables at two and higher loop levels \([8]\).

The model employed here has two free parameters, the coupling constants \( \lambda_s \) and \( \lambda_S \), both hiding the explicit dependence on the singlet mass \( m_s \) and Higgs mass \( m_h \). The first parameter is constrained to be around \( \lambda_s \lesssim 10^{-8} \) by the current GRBs BATSE observations, and its value will be measured at the \( \gamma\gamma \) mode of the TESLA collider \([3]\). As a final remark, the potential realization of this scenario in the astrophysical sources triggering GRBs would render it a viable pathway for testing some of the extensions of the standard model of particle physics introduced to account for the overall GRBs observational properties: energetics, timescales, spectra, etc., such as the one being suggested here.

ACKNOWLEDGMENTS

We would like to thank A. Dar, A. Kusenko, S. Nussinov and A. Yu. Smirnov for helpful suggestions and fruitful discussions on this work.

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