Micro-Motion Feature Extraction of a Rotating Target Based on Interrupted Transmitting and Receiving Pulse Signal in an Anechoic Chamber

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Abstract: The pulse signal is widely used in micro-motion feature extraction of rapidly rotating targets as its pulse repetition frequency (PRF) can be high. However, when the pulse signal is implemented in a range-limited anechoic chamber for micro-motion feature extraction, the transmitted and reflected pulse signals may be coupled at the receiver. To solve this problem, the interrupted transmitting and receiving (ITR) method is applied to transmit the pulse signal with hundreds of sub-pulses. The target echo can be received when the sub-pulse is not transmitted. Hence, it avoids the coupling effect of transmitted signals and echoes. Then, the whole process of micro-motion feature extraction for rotating target is proposed based on the ITR method. At last, the simulations and experiments verify that the rotating target micro-Doppler can be extracted by the ITR pulse signal.

Keywords: pulse radar; rotating target; micro-motion feature extraction; interrupted transmitting and receiving (ITR)

1. Introduction

Radar target feature extraction is widely investigated for automatic target recognition [1,2]. The micro-motion feature is one of the most important features [3–5]. In the past decades, the micro-motion feature measurement in an anechoic chamber has been conducted via the swept frequency signal [6]. Firstly, the target is placed on the turntable at a certain angle. Then, the swept frequency signal is transmitted to the target, and the scattering field data at the specific aspect angle is obtained. The static measurement is conducted with the turntable turning in different aspect angles. Therefore, in order to obtain precise measurement results, the angle interval of the turntable should be small enough which results in a long measurement time. Besides, the pulse repetition frequency (PRF) of the swept frequency signal in [7] is small for micro-motion feature extraction. As a result, the micro-Doppler of the rapidly micro-motional target may be aliasing. Thus, the micro-motion feature cannot be extracted in this case.

Pulse signal is extensively used in target detection and recognition [8]. As a high PRF of the pulse signal can be achieved [9,10], it can be used in the rapid micro-motion feature extraction of micro-motional target. Then, the turntable turns continuously so that the dynamic measurement of micro-motional target can be implemented in the anechoic chamber. For pulse signal, the target has to be located in the unambiguous range so that it can be detected. However, the size of the anechoic chamber is relatively small in comparison with field experiments, and usually smaller than the minimum unambiguous range. Consequently, the pulse signal is difficult to be used in the anechoic chamber measurement directly. The inner reason is that the target echoes are received while the pulse
is not completely transmitted. At this time, the transmitted and received pulse signal are coupled at
the receiver [11], therefore, the received pulse signal is affected by the transmitted signal. Various
wave cancellation methods have been discussed, such as acoustic cancellation [12,13] and radar echo
cancellation [14]. However, as the transmitted and received pulse signals are relevant, they are difficult
to be separated by the echo cancellation.

In order to conduct the micro-motion feature extraction in anechoic chamber with pulse radar
signal, the whole procedure of target measurement is proposed in this paper based on the interrupted
transmitting and receiving (ITR) [11,15,16]. Firstly, the pulse radar signal is transmitted and received
in sub-microseconds to obtain the target echoes. Then, the target echo property is discussed in detail.
The micro-motion extraction procedure based on time-frequency analysis [17,18] is provided and
analyzed with experimental results.

The remainder of the paper is organized as follows. Section 2 discusses the principle of ITR for
pulse radar signal and the characteristics of ITR echo. In Section 3, the procedure of micro-motion
feature extraction for rotating target is provided based on the ITR echo. In Section 4, both simulation
and experiment results in anechoic chamber are provided with different ITR control parameters to
validate of the proposed rotating feature extraction method. Finally, some conclusions are drawn in
Section 5.

2. Characteristics of Interrupted Transmitting and Receiving Echo

2.1. Principle of ITR

As discussed in [11] and [16], ITR means that the antenna is turned on to transmit the pulse signal
in sub-microseconds and then interrupted. After that, the other antenna is turned on to receive the
echo. Repeating the above procedures for hundreds of times, the whole pulse is fully transmitted. As a result, the complete pulse signal is divided into hundreds of sub-pulses as shown in Figure 1.

![Figure 1. Waveform of p(t).](image)

The ideal signal to control the transmitting and receiving can be expressed as

\[
p(t) = \text{rect}(t/\tau) \ast \sum_{n=-\infty}^{+\infty} \delta(t - nT_s)
\]  

(1)

where \( \delta(t) \) is the impulse function, \( n \) is the pulse number, \( T_s \) is the period, \( \ast \) represents the convolution operation, and \( \text{rect}(t/\tau) \) is the rectangular envelope as follows

\[
\text{rect}(t/\tau) = \begin{cases} 
1, & |t/\tau| < 0.5 \\
0, & \text{others}
\end{cases}
\]

(2)

where \( \tau \) is restricted to sub-microsecond to ensure the sub-pulse be fully transmitted before it returns
to the receiver in anechoic chamber. In practice, \( \tau \) should be designed according to the real size of the
anechoic chamber at first.

The spectrum of \( p(t) \) is

\[
P(f) = \tau f_s \sum_{n=-\infty}^{+\infty} \sin c(n f_s \tau) \delta(f - n f_s)
\]

(3)

where \( f_s = 1/T_s \), and \( \sin c(x) = \sin(\pi x)/\pi x \).
2.2. Property of ITR Echo

Assuming the operated pulse signal is linear frequency modulated (LFM) signal and it can be written as

$$s(t) = \text{rect} \left( \frac{t}{T_p} \right) \exp \left[ j2\pi \left( f_c t + \frac{1}{2} \mu t^2 \right) \right]$$

where $f_c$ is the carrier frequency, $T_p$ is the pulse width, $\mu$ is the chirp rate, and the bandwidth is $B = \mu T_p$.

The de-chirp reference signal is

$$s_{\text{ref}}(t) = \text{rect} \left( \frac{t - 2R_{\text{ref}}/C}{T_{\text{ref}}} \right) \exp \left( j2\pi \left( f_c \left( t - \frac{2R_{\text{ref}}}{C} \right) + \frac{1}{2} \mu \left( t - \frac{2R_{\text{ref}}}{C} \right)^2 \right) \right)$$

where $R_{\text{ref}}$ is the reference range, $T_{\text{ref}}$ is the pulse width of reference signal, and $C$ is the electromagnetic wave velocity.

After de-chirping with the reference signal, the difference-frequency output is

$$s_f(t) = s_r(t)s^*_\text{ref}(t)$$

where $s^*_\text{ref}(t)$ is the conjugation of $s_{\text{ref}}(t)$, and $s_r(t)$ is the echo which can be expressed as

$$s_r(t) = \sum_{k=1}^{K} \alpha_k s(t - 2R_k/C)$$

where $K$ is the number of scattering centers, $\alpha_k$ is the scattering coefficient, and $R_k$ is the distance between the scattering center $k$ and radar.

Then, the ITR echo is obtained as

$$s_{\tau_2}(t) = p_2(t) \cdot s_r(t) = \left( \text{rect} \left( \frac{t}{\tau} \right) * \sum_{n=-\infty}^{+\infty} \delta(t - nT_s) \right) s_r(t)$$

The high-resolution range profile (HRRP) of ITR echo can be obtained after fast Fourier transform (FFT)

$$S_{f_s}(f) = \tau f_s T_p \sum_{k=1}^{K} \alpha_k \exp \left( -j \frac{4\pi f_c}{C} R_{k,\Delta} \right) \sum_{n=-\infty}^{+\infty} \sin c(n f_s \tau) \sin c \left( T_p \left( f - n f_s + 2 \frac{\mu}{C} R_{k,\Delta} \right) \right)$$

where $R_{k,\Delta} = R_k - R_{\text{ref}}$.

From (9), we can find that the amplitude is related to $\tau$, $f_s$, and $T_p$. The second item sinc() in the summation operation illustrates that the de-chirp output is the accumulation of different sinc() functions. Besides, there are different orders of fake peaks in HRRP with the frequency interval $f_s$ and the distance between the real and fake peaks is $\Delta R = C f_s/(2\mu)$.

Therefore, the real peaks in HRRP can be fully obtained if $L < \Delta R$, where $L$ is the target length. And then

$$T_s < \frac{C}{2\mu L}$$

3. Micro-Motion Feature Extraction of the Rotating Target

3.1. The Micro-Doppler of the Rotating Target

With the increasing complexity of target structure, many targets contain rotating components, such as aircraft propellers. The distance between the scattering centers and radar varies periodically
with time, which produces the particular Doppler shift. Figure 2 shows the typical rotating target structure. Scattering centers A and B are both located at the line apexes and the location of which remains unchanged with the rotation. According to the scattering center classification [19,20], A and B are localized scattering centers which usually correspond to the geometric discontinuities such as corners, edge apexes, cone tips, and so on.

![Figure 2. The typical rotating target structure.](image)

Generally, the stop-and-go approximation is adopted, and the position of scattering center is basically unchanged in the fast time. In the slow time $t_m$, the distance between point A and radar can be expressed as

$$R_A(t_m) = R_0 - r \cos(2\pi f_p t_m + \phi_0) \quad (11)$$

where $R_0$ is the distance between reference scattering center O and radar, $r$ is the rotation radius, $f_p$ is the rotation frequency and $\phi_0$ is the initial phase.

According to (9), the HRRP of the ITR echo including micro-motion information can be obtained as

$$\hat{S}_{f_s}(f, t_m) = \tau f_s T_p \sum_{k=1}^{K} \alpha_k \exp\left(-\frac{4\pi f_s}{\lambda} R_{k,A}(t_m)\right) \cdot \sum_{n=-\infty}^{+\infty} \sin c(n f_s \tau) \sin c\left[T_p \left(f - n f_s + 2\frac{\mu}{C} R_{k,A}(t_m)\right)\right] \exp\left(-\frac{4\pi n f_s}{C} R_{\text{ref}}\right) \quad (12)$$

When $n = 0$, the peak value of HRRP in (9) is

$$\hat{S}'_{f_s}(f, t_m) = \tau f_s T_p \sum_{k=1}^{K} \alpha_k \exp\left(-\frac{4\pi f_s}{C} R_{k,A}(t_m)\right) \sin c\left[T_p \left(f + 2\frac{\mu}{C} R_{k,A}(t_m)\right)\right] \quad (13)$$

where $R_{k,A}(t_m) = R_k(t_m) - R_{\text{ref}}$.

Then, the phase term in (13) is

$$\phi_k(t_m) = -\frac{4\pi}{\lambda} R_{k,A}(t_m) \quad (14)$$

where $\lambda = C/f_s$ is wavelength.

Therefore, the Doppler frequency of point A is obtained as

$$f_{\text{micro},A} = \frac{1}{2\pi} \frac{d\phi_A(t_m)}{dt_m} = \frac{4\pi f_p}{\lambda} \sin(2\pi f_p t_m + \phi_0) \quad (15)$$

After time-frequency analysis with (13), the Doppler frequency of point A can be extracted, which is the result of Equation (15).

3.2. Procedure of the Micro-Doppler Extraction with ITR

Based on the above analysis, the whole procedure of micro-motion feature extraction for rotating target is given in Figure 3.
According to Figure 3, the target echo is received with ITR, and then the target HRRP is obtained by de-chirp processing. After selecting the peak position of target HRRP, the time-frequency analysis can be conducted along the slow time. There are many candidate time-frequency methods such as wavelet transform, Wigner–Ville distribution, short-time Fourier transform (STFT), and so on. Due to simplicity, STFT is chosen in this paper. Finally, the micro-motion information of rotating scattering center can be obtained.

4. Simulation and Experiment Results

4.1. Simulation Results of Rotating Target Micro-Doppler Extraction

The PRF of typical pulse radar signal may vary from hundreds of Hertz to hundreds of thousands of Hertz [9,10]. Therefore, the dynamic measurement of target with high rotation rate can be accomplished by the high PRF of pulse radar signals.

As shown in Figure 2, the typical rotating target echo is simplified as two scattering centers, A and B. The distance between the two scattering centers is \(2r = 0.2\) m. They are rotating around the midpoint \(O\) at a frequency of 8 Hz. The slant range between the midpoint \(O\) and radar \(R_0\) is 45 m. The parameters of radar are listed in Table 1.

| Parameter | Value | Parameter | Value |
|-----------|-------|-----------|-------|
| Pulse width \(T_p\) | 12 \(\mu\)s | Bandwidth \(B\) | 500 MHz |
| PRF | 1.67 kHz | ITR period \(T_s\) | 0.6 \(\mu\)s |
| Wave length \(\lambda\) | 0.03 m | ITR pulse width \(\tau\) | 0.2 \(\mu\)s |

In Table 1, the bandwidth of the pulse signal and swept frequency signal is 500 MHz. As the pulse width is 12 \(\mu\)s, the distance between the real and fake peaks is 6 m according to \(\Delta R = Cf_s/(2 \mu)\). Because the target rotation radius is 0.1 m, and the target length is 0.2 m so that the real and fake peaks can be separated. Moreover, the ITR pulse width \(\tau\) should be smaller than \(2R/C\) so that the sub-pulse can be fully transmitted when the reflected signal returns. Because the distance between the target and radar is \(R = 45\) m, \(\tau\) is set as 0.2 \(\mu\)s which is smaller than \(2R/C = 0.3\) \(\mu\)s.

The PRF of swept frequency signal is set as 68 Hz for comparison since the equivalent PRF of the swept frequency experimental system is 68 Hz in [7]. The swept frequency interval is 1 MHz and the signal bandwidth is 500 MHz.

Firstly, the typical rotating target echo is simulated with swept frequency signal so that the HRRP can be obtained. According to Equations (7) and (8), the complete pulse echoes and ITR echoes are obtained. Then, the corresponding HRRPs are calculated via FFT. At last, the time-frequency analysis is conducted to extract micro-motion features based on the HRRPs. The micro-Doppler extraction results are shown in Figure 4.

Figure 4a is the range slow-time image obtained by the complete pulse echo. Figure 4b is the micro-Doppler extraction result of the complete pulse echo, in which the micro-Doppler frequency is obtained accurately, and it is the ideal result. Figure 4c is the range slow-time image obtained by
the swept frequency signal. Figure 4d is the micro-Doppler extraction result of the swept frequency signal. Because of the PRF of swept frequency signal is small, i.e., $f_{\text{micro},A} > \text{PRF}/2$, the extracted micro-Doppler frequency is aliased. Figure 4e is the range slow-time image obtained by the ITR echo. According to (10), the ITR period $T_s$ is smaller than 18 µs, therefore, the real peaks can be extracted by adding a suitable interception window in the HRRP. Then, the time frequency analysis is performed to extract the micro-Doppler. We found that the micro-Doppler information depicted in Figure 4f is basically consistent with that in Figure 4b. In addition, the maximum amplitude values in Figure 4e,f is less than those in Figure 4a,b as depicted in the color bar. It is because the echo energy is reduced after ITR. However, the amplitude reduction can be eliminated by energy compensation.

Figure 4. Micro-Doppler extraction results. (a) Range slow-time image of the complete pulse echo. (b) Time-frequency image of the complete pulse echo. (c) Range slow-time image of the swept frequency echo. (d) Time-frequency image of the swept-frequency echo. (e) Range slow-time image of the ITR echo. (f) Time-frequency image of the interrupted transmitting and receiving (ITR) echo.
4.2. Experiment Results in Anechoic Chamber

In this section, the pulse radar signal ITR experimental system is established for rotating target micro-motion extraction. The experimental system and the rotation target are shown in Figure 5.

![Experimental system and rotation target model.](image)

(a) The experiment scenario.

![Experimental system.](image)
(b) The experimental system.

![Horn antennas.](image)
(c) The horn antennas.

![Rotation target.](image)
(d) The rotation target.

**Figure 5.** Experimental system and rotation target model. (a) The experiment scenario. (b) The experimental system. (c) The horn antennas. (d) The rotation target.

The micro-motion feature measurement experimental scenario is presented in Figure 5a. The compact range reflector is used to ensure the plane wave. The width and length of the anechoic chamber are almost 15 m and 20 m, respectively. In this case, the pulse width should be smaller than 0.13 μs at the least to eliminate the coupling effect of the transmitted and reflected signal. Hence, the use of the ITR method is necessary. As shown in Figure 5b, the ITR experimental system is composed of three parts. Part A contains the local oscillator, arbitrary waveform generator (AWG), ITR controller, down-conversion (DC) module and intermediate frequency adjustment module. Part B is the vector signal generator (VSG) to up-convert the intermediate frequency signal. Part C is the intermediate frequency digitizer for data acquisition. Figure 5c shows the transmitter and receiver horn antennas. The intermediate-frequency LFM signal of 300 MHz is generated by the AWG. Then, the signal is up-converted by the VSG to 9.3 GHz and the antenna radiates the signal to target by ITR antenna controller. Target echo is down-converted by the DC module. After intermediate frequency adjustment, the echo can be stored by the intermediate frequency digitizer module. Finally, the ITR echo is processed on the computer.

In Figure 5d, two corner reflectors are placed at the end of the cross bar to simulate the rotating scattering centers. The rotation is controlled by the motor and the rotation rate of the motor needs to be manual controlled during the experiment. The experimental parameters are listed in Table 2.

According to the procedure in Figure 3, when \( B = 10 \text{ MHz} \) and the rotation rate is about 0.85 s, the results of micro-Doppler extraction are drawn as follows. The maximum rotation frequency of the corner reflector is extracted by time frequency distribution–Hough (TFD–Hough) transformation \([21,22]\).

The HRRP of ITR echo is shown in Figure 6b. Then, the range slow-time image can be obtained in Figure 6c. After extracting the target peaks in HRRP, time-frequency analysis can be conducted in the slow time domain to obtain the time-frequency image in Figure 6d. It can be found that two sinusoidal curves with the same period and opposite initial phases are presented in the time-frequency image,
which illustrates the micro-Doppler of the two corner reflectors. According to the time-frequency image, the micro-Doppler period is about 0.86 s, which is well consistent with the rotation period 0.85 s set in the experiment. At the same time, when \( r = 0.38 \text{ m}, \lambda = 0.03 \text{ m}, \) and \( f_p = 1/0.85 \text{ s} = 1.18 \text{ Hz}, \) the theoretical maximum micro-Doppler frequency of the corner reflector is \( 187.26 \text{ Hz} \) according to (15). The maximum frequency in the time-frequency image is \( 185.09 \text{ Hz} \), which is also consistent with the calculation results.

| Table 2. Parameter setting of uniform transmitting and receiving period for rotating target. |
|---------------------------------------------|---------------------------------------------|
| Parameter          | Value           | Parameter          | Value           |
|---------------------|-----------------|---------------------|-----------------|
| Pulse width \( T_p \) | 12 \( \mu \text{s} \) | bandwidth \( B \) | 10 MHz          |
| PRF                 | 1 kHz           | ITR period \( T_s \) | 0.4 \( \mu \text{s} \) |
| Wave length         | 0.03 m (10 GHz) | ITR pulse width \( \tau \) | 0.1 \( \mu \text{s} \) |
| Target range        | 15.5 m          | rotation radius     | 0.38 m          |

When the rotation period is 1.1s and \( B = 300 \text{ MHz} \), the micro-Doppler extraction results are shown in Figure 7.

The HRRP of ITR echo is shown in Figure 7b. As the signal bandwidth increases, the range resolution is \( C/(2B) = 0.5 \text{ m} \) so that the two reflectors can be distinguished by HRRP in Figure 7c. The range slow-time 2D image is obtained in Figure 7d,e. It can be seen that the periodic characteristic of HRRP is clear in Figure 7e. When the two reflectors are in the same range cell, the scattering points cannot be separated in the HRRP. Time-frequency analysis is conducted by selecting this range cell and the time-frequency image is obtained as presented in Figure 7f. Comparing Figure 7e,f, when two scattering points are in the same range cell, the corresponding micro-Doppler frequency is maximum.
In addition, according to the time-frequency image and range slow-time 2D image, the target rotation period is about 1.122 s and the maximum micro-Doppler frequency is 141.87 Hz. The rotation rate is set as 1.1 s, and the maximum micro-Doppler frequency calculated by (15) is 144.7 Hz, which are all consistent with the experiment results.

Figure 7. The ITR echo and micro Doppler extraction results ($B = 300$ MHz, $T_s = 0.4$ µs). (a) The ITR echo. (b) HRRP of ITR echo. (c) Magnification of HRRP. (d) Range slow-time 2D image. (e) Magnification of Range slow-time 2D image. (f) Time-frequency image.

5. Conclusions

The whole procedure for the micro-motion feature extraction of rapid micro-motional target is proposed based on the ITR method. The ITR is firstly applied to obtain the target echo in the anechoic chamber. Then, the HRRP of rotating target is deduced with the ITR echo. After that, the target range cell is selected for target micro-Doppler extraction. At last, numerical simulations and experiments in the anechoic chamber are conducted, which verify the validity of the proposed method.

In future, the dynamic measurements of more complicated micro-motional target will be discussed with the proposed method. We will also investigate the echo reconstruction method which makes the ITR echoes approximate the complete pulse echoes as much as possible.

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