Strain evolution of each type of grains in poly-crystalline (Ba,Sr)TiO₃ thin films grown by sputtering

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The strain states of [111]-, [110]-, and [002]-oriented grains in poly-crystalline sputtered (Ba,Sr)TiO₃ thin films on highly [111]-oriented Pt electrode/Si substrates were carefully examined by X-ray diffraction techniques. Remarkably, [002]-oriented grains respond more while [110]- and [111]-oriented grains do less than the theoretically estimated responses, which is understandable from the arrangement of the TiO₆ octahedra with respect to the stress direction. Furthermore, such mechanical responses are completely independent of the degree of crystallization and film thickness. The transition growth temperature between the positive and negative strains was also different depending on the grain orientation. The unstrained lattice parameter for each type of grain was different suggesting that the oxygen vacancy concentration for each type of grain is different, too. The results reveal that polycrystalline (Ba,Sr)TiO₃ thin films are not an aggregation of differently oriented grains which simply follow the mechanical behavior of single crystal with different orientations.

The mechanical properties of materials are one of the fundamental material parameters, which are generally represented by the relationship between the strain (\(\varepsilon\)) and stress (\(\sigma\)). Sometimes, the \(\varepsilon\) and \(\sigma\) influence other fundamental properties of the materials, such as the electrical properties (piezoelectric effect) and defect distribution (piezochemical effect), as well as the mechanical response of the materials. Perovskite structured materials are a typical example showing such a correlation between the different fundamental properties due to their high ionic polarizability. Many perovskite oxide thin films, such as (Ba,Sr)TiO₃ (BST), showed a crucial influence of the \(\varepsilon\) and accompanying \(\sigma\) on the functionality of the films, such as the dielectric constant, polarization, Curie temperature, and piezoelectric coefficient¹⁰. The strain can even transform the non-ferroelectric phase to the ferroelectric phase and vice versa¹¹. Recent theoretical calculations indicated that the strain also provides an important contribution to the dielectric and ferroelectric properties of the perovskite oxide/metal interfaces, which mostly govern the functionality of the nano-meter scale thin films¹²–¹十四.

The strain in thin films is induced by various intrinsic factors, such as the misfit strain and the thermal expansion mismatch with the substrate, as well as extrinsic factors, such as the impurity/vacancy incorporation and shot-peening effect in sputtering¹⁵. In many cases, many of these factors simultaneously influence the strain state of the perovskite oxide films, which renders the fundamental understanding on the influence of these factors on the properties of the films complicated and often disagree with the theoretical expectations.

The recent development in the fabrication techniques for the epitaxial perovskite oxide thin films¹⁶–²⁰ has greatly improved the experimental verification for the influence of the strain. However, the epitaxial systems often have limited usefulness regarding their use in many important applications, such as random access memory devices and integrated electro-mechanical systems, which are usually formed on Si substrate for commercial reasons. Si is very vulnerable to the chemical reaction and poorly lattice-matched with these perovskite oxides. Its thermal expansion mismatch is also non-favorable for improving the functionality. Due to these non-desirable factors of Si substrate, it is usually passivated with amorphous SiO₂ films and a poly-crystalline bottom electrode, typically Pt, which inevitably results in poly-crystalline perovskite thin films.

It must be quite a natural consequence that the strain state of the poly-crystalline film has a much more complicated pattern due to the non-uniform structure and crystallographic direction of each grain. It appears that there are two fundamental questions regarding the strain status of poly-crystalline films; what is the strain state of...
each grain, and is the strain state of each grain influenced by the strain state of neighboring grains? The other question is what is the defect (typically oxygen vacancy) concentration in each grain and does this have a certain relationship with the strain state of each grain? These questions are difficult to answer even when using the state-of-the-art spectroscopic tools having high spatial resolutions since the defect concentrations are generally very low.

In this report, the authors attempted to answer these two important questions by adopting the X-ray diffraction (XRD) technique to the poly-crystalline BST thin films with a thickness of 120 nm which were deposited on highly [111]-orientation preferred poly-crystalline Pt thin film electrodes by an rf magnetron sputtering technique at substrate temperatures \( T_s \) ranging from 338 to 505 °C. The different \( T_s \) results in the different stress state of the films; low and high \( T_s \) induced the overall in-plane compressive and tensile stresses, respectively, due to the dominance of the shot peening effect (at low \( T_s \)) and the mismatch in the thermal expansion coefficients of Si substrate and BST film (at high \( T_s \)). In addition, BST films with thicknesses ranging from 29.6 to 155.8 nm were deposited at 505 °C in order to understand the influence of the film thickness on the stress and defect states of each grain. The strain state of each grain with different orientations was estimated by a careful XRD analysis using the sin\(^2\)ψ method. The results are compared with the expected strain-stress relationship from the bulk compliance values. Semi-quantitative discussions on the reason for the evolution of different stress-strain states based on the crystal structure of the perovskite material are presented.

**Results**

First, the influences of \( T_s \) on the structural properties of BST films are discussed. Experimental details and detailed information on the accurate thickness and cation compositions of each BST film are shown in the methods section and in on-line supplementary information (table SI), respectively. The films are usually slightly Ti-rich (Ti/(Ba+Sr+Ti) ~ 0.52) and Ba-deficient (Ba/(Ba+Sr) ~ 0.48). XRD spectra in Θ-2Θ mode of the BST films showed relatively random growth directions with (110), (111) and (002) peaks. Although the diffraction peak intensity generally increases with the increasing \( T_s \), suggesting better crystalline quality and less mosaicity, the relative peak intensity ratio did not vary significantly. (See Fig. S1 of on-line supplementary information) The peak position generally shifts into the high 2Θ direction with the increasing \( T_s \), suggesting that the films undergo more in-plane tensile stress due to the thermal expansion mismatch between the BST (\( \sim 10 \times 10^{-6} \text{ °C}^{-1} \)) and the Si substrate (\( \sim 2.62 \times 10^{-6} \text{ °C}^{-1} \)) while cooling down after the film deposition. Detailed strain evolutions for each type of grain in the different films were examined by the sin\(^2\)ψ method. Here ψ is the angle between the direction normal to the film surface and the direction of the specific crystallographic orientation where the inter-planar spacing was measured (ex, (112), (110), and (−112) planes for the [111]-oriented grains). Details for the sin\(^2\)ψ method can be found from Ref. 23 and its principle can be represented by Eq. (1) shown below.

\[
\sqrt{h^2 + k^2 + l^2} = \sqrt{\tilde{h}^2 + \tilde{k}^2 + \tilde{l}^2} \{e_\psi (\omega_0 - \omega_\psi) \sin^2 \psi + a_\psi (\omega_0 - \omega_\psi) \sin^2 \psi + a_\psi (\omega_0 - \omega_\psi) (\omega_0 + \omega_\psi) + 1 \}
\]

where, \( h, k, l, d_\psi, \tilde{h}, \tilde{k}, \tilde{l}, \omega_0, \omega_\psi \) are the three Miller indices, measured inter-planar spacing at the measurement angle \( \psi \), and the calculated out-of-plane inter-planar spacing (\( \psi = 0 \)), strain along the measurement direction \( \psi \), in-plane strain, and out-of-plane strain, respectively. \( d_\psi \) and \( a_\psi \) are measured lattice parameters at the measurement angle \( \psi \), and the calculated out-of-plane lattice parameter (\( \psi = 0 \)). The positive and negative slopes correspond to in-plane tensile (\( \sigma_\psi > 0 \), i.e. \( \omega_0 > \omega_\psi \)) and compressive (\( \sigma_\psi < 0 \), i.e. \( \omega_0 < \omega_\psi \)) stress states, respectively. From the extrapolation of the linear

![Figure 1](image)

**Figure 1** Variations in the lattice parameters of (a) the Pt electrode film, (b) [002]-, (c) [110]-, and (d) [111]-oriented BST grains as a function of sin\(^2\)ψ for the BST films grown at different \( T_s \).
fitting to $\sin^2 \psi = 1$ and 0, $\varepsilon_0$ and $\varepsilon_2$ can be estimated for each sample. There are several notable findings from the data sets shown in Fig.1 which could be more evidently seen in Fig. 2.

Figures 2a-d show the variations in the $\varepsilon_0$ and $\varepsilon_2$ values as well as the variation of the effective Poisson’s ratio, $\nu (= -\varepsilon_2/\varepsilon_0)$, of the Pt film and those of the three differently oriented BST grains as a function of $T_s$. In this paper, the positive and negative strains denote the tensile and compressive strains, respectively. The Pt film has only [111]-oriented grains and shows in-plane positive strain at all $T_s$ due to the thermal expansion mismatch with Si (thermal expansion coefficient of Pt ~ 9.6 x 10^-6 °C^-1). However, the BST films show complicated development of strains depending on the $T_s$ and types of grains. The [002]- and [110]-oriented grains grown at 505 °C show in-plane positive strain, but the same type of grains grown at lower $T_s$ show in-plane negative strains. The cross-over from the positive to negative strain occurs at ~ 460 °C. After the abrupt change in the strain state near the transition temperature, the negative strain further develops rather slowly with the decreasing $T_s$ for the [002]-oriented grains. However, that of [110]-oriented grains are rather complicated, which is not yet clearly understood. In addition, the magnitudes of $\varepsilon_0$ and $\varepsilon_2$ are symmetric and generally high in [002]-oriented grains due to the higher compliance $(S_{11})$ and high $v$ along [002] direction. Nevertheless, they are rather asymmetric in [110]-oriented grains along the tensile and compressive directions probably due to the different crystallographic structures. [111]-oriented grains also show in-plane positive strain at the highest $T_s$ but with a smaller magnitude of in- and out-of-plane strains. Interestingly, the transition into the negative strain state occurs at much lower $T_s$ (~ 400 °C). Therefore, the [111]-oriented grains demonstrate an in-plane negative strain state only at the lowest $T_s$ with a much smaller magnitude of $\varepsilon_0$ and $\varepsilon_2$. For this case, the magnitude of $\varepsilon_2$ is generally smaller than that of $\varepsilon_0$. The variations in $v$ appears to be related with the strain state in Figs. 2 (b) and (c), but it is not the case in Fig. 2 (d). Such variations in $v$ are actually related with the change in Ba/Sr ratio with the varying $T_s$, and the relative comparison with the theoretically calculated values for the given Ba/Sr ratio has a higher significance as discussed below.

The in-plane tensile stress (positive strain) in BST grains can be generally understood from the thermal expansion mismatch between the film and Si substrate. The influence of Pt and SiO$_2$ films is negligible due to their much thinner thickness (~ 0.1 μm) compared to that of Si substrate (~ 600 μm). The higher in-plane tensile stress state at higher $T_s$ can be understood from the thermal effect. The in-plane compressive stress (negative strain) in BST films could be understood from the shot-peening effect. The energetic bombardment of the sputtered particles (especially negatively charged oxygen ions) onto the growing film surface imparts the in-plane compressive stress. Therefore, the increasing in-plane negative strain with the decreasing $T_s$ can be understood from the domination of the ion bombardment effect of the sputtering process over the thermal expansion mismatch. Given the low compliance along the [111] direction of the perovskite BST material, the out-of-plane strain ($\varepsilon_2$) of the [111]-oriented grains must be smallest at the lowest $T_s$ (338 °C), which is indeed the case as shown in Fig. 2d. The same argument can be applied to the in-plane tensile cases; out-of-plane negative strain along the [111] direction is quite small at 505 °C, due to the lower in-plane tensile strain at the same temperature compared to the other types of grains. In addition, the lower evolution of compressive stress by the larger decrement of the shot-peening effect in [111]-oriented grains compared to the grains with different orientations decreases the transition temperature from ~ 460 to ~ 400 °C. In other words, the thermal effect dominates the mechanical bombardment effect even at lower $T_s$ in [111]-oriented grains. These results must be a natural consequence of the crystallographic-direction specific mechanical properties of the BST material; lower and higher compliance along the [111] and [002] orientations, respectively. (See online supplementary information for the calculation along different directions, and the text below for more discussions. The calculated values are included in Table I.)

In order to confirm whether the different responses of each type of grain to the external stress coincides with the bulk properties of the material, $v$ under biaxial stress was calculated for the different orientations of the crystals where in-plane biaxial stress $(\sigma_{0})$ was applied to the isolated [111], [110], and [002]-oriented gains, respectively, and the results are compared with the experimental results. These calculations were based on the elastic theory of cubic crystal and compliance tensors of the material with the same cation composition. It has to be noted that each type of grain must have a completely random in-plane orientation for this comparison to hold its validity, which was indeed the case for [111]- and [002]-type grains but not for [110]-type grains (See Fig. 3), because the film is of the polycrystalline nature. Table I shows the variations in the calculated compliance $(\varepsilon_0/\sigma_0$ and $\varepsilon_2/\sigma_0$), and the $v$ of the crystal with the [111], [110], and [002] directions normal to the stress plane, as well

**Figure 2** | Variation of in-plane and out-of-plane strain as a function of substrate temperature of (a) [111]-oriented grain of Pt, and those of (b) [002]-, (c) [110]-, and (d) [111]-oriented grains of the (Ba,Sr)TiO$_3$ thin films.
as the \( n \) measured experimentally for the three different types of grain of the BST films grown at the various \( T_s \). Due to the slightly different compositions of the different samples, Ba/Sr ratio of the films grown at 338, 402 and 431 °C was taken as 48/52, and that of the other two samples was taken as 47/53.

It is notable that the measured \( n \) of each type of grains is completely independent of \( T_s \) for the given Ba/Sr ratio, suggesting the identical mechanical responses of the different grains irrespective of the crystalline quality of the polycrystalline BST films. For the [002]-oriented grains, the measured \( n \)'s are generally larger than the theoretically calculated values, suggesting that these grains have higher strains than the theoretically expected values along the out-of-plane direction. In contrast, the measured \( n \) of the [110]- and [111]-oriented grains is smaller than the theoretical value, suggesting that these grains strain less along the out-of-plane direction. In fact, there are several data sets on the value of compliances of BaTiO3 and SrTiO3, from which the compliance values of 48/52 and 47/53 materials are calculated (see table S III of online supplementary information). Therefore, the theoretical \( n \)'s are certainly with some degree of uncertainty. However, the relative comparison between the measured and calculated values is certainly correct. Such a discrepancy between the theoretical and measured values of the \( n \)'s and different relative tendency suggest the following. The differently oriented grains experience a significant mechanical confinement effect due

| Table I | Comparison between the calculated and experimental Poisson’s ratio for 120-nm-thick (Ba,Sr)TiO3 films with Ba/Sr ratio of 48/52 and 47/53, respectively |
|---------|---------------------------------------------------------------------------------------------------------------|
| Ba/Sr = 48/52 |                                                                                                           |
|          | \( \varepsilon_0 / \sigma_0 \) | \( \varepsilon_z / \sigma_0 \) | \( -\varepsilon_z / \varepsilon_0 \) | Calc. | Meas. (at 338 °C) | Meas. (at 402 °C) | Meas. (at 431 °C) |
| [002]    | 4.076 | -3.476 | 0.853 | 0.947 | 0.947 | 0.947 |
| [110]    | 3.254 | -1.832 | 0.563 | 0.531 | 0.531 | 0.531 |
| [111]    | 2.980 | -1.284 | 0.431 | 0.344 | 0.344 | 0.344 |

| Ba/Sr = 47/53 |                                                                                                           |
|              | \( \varepsilon_0 / \sigma_0 \) | \( \varepsilon_z / \sigma_0 \) | \( -\varepsilon_z / \varepsilon_0 \) | Calc. | Meas. (at 462 °C) | Meas. (at 505 °C) |
| [002]        | 4.047 | -3.439 | 0.850 | 0.942 | 0.942 |
| [110]        | 3.240 | -1.824 | 0.563 | 0.454 | 0.454 |
| [111]        | 2.971 | -1.286 | 0.433 | 0.342 | 0.342 |

Figure 3 | (a) [111] pole figure of Pt substrate, and (b) [111] pole figure, and (c) [110] pole figure of (Ba,Sr)TiO3 thin films.
to the densely packed columnar microstructure (see fig. S2 of on-line supplementary information for cross-section transmission electron microscopy image) and smaller strain of the [110]- and [111]-oriented grains to the external biaxial stress is compensated by the larger strain of the [002]-oriented grains.

Figure 3 shows the pole figures of [111]-oriented Pt electrode grains (3a, where in-plane distribution of (11-1) type plane is shown), [110]-oriented BST grains (3b, where in-plane distribution of (111) type plane is shown), and [111]- and [002]-oriented BST grains (3c, where in-plane distribution of (110) type plane is shown). The randomness of the in-plane distribution for Pt grains is almost perfect as can be understood from the almost constant distribution of the (11-1) X-ray diffraction peak intensity along the \( \phi \) angle. This was also the case for the [111]- and [002]-oriented grains so that the (110) X-ray diffraction peak intensities along the \( \phi \) angle are almost constant. However, the [110]-oriented grains have a much more non-random in-plane orientation compared to the other cases. Although the exact reason for such an extraordinary behavior is not clearly understood, it was related with the highly anisotropic nature along the crystallographic directions on the (110) plane compared to the more isotropic nature of the (111) and (002) planes. This may explain the peculiar variations in \( e_c \) and \( e_o \) of this type of grain shown in Fig. 2c. However, it appears that such a discrepancy in the degree of randomness of the in-plane orientation does not influence the mechanical confinement effect largely.

The different mechanical responses of the different types of grains, shown in Fig. 2, can be understood from the calculated compliance values and Poisson’s ratio along the different directions of the bulk crystal shown in Table 1. The absolute value of the out-of-plane compliance along the [111] is the smallest and that along the [002] is the largest. The possible reasons for such a discrepancy was considered from the possible distortion of the TiO$_6$ octahedra, which are the building blocks of the BST material in response to the external stress, and the results are included in the Fig. S3 of on-line supporting information. Due to the different compliance values along the different crystallographic directions, the different types of grains respond differently to the mechanical stress along the in-plane direction; under the given (in-plane) compressive stress, for example, the smaller compliance of the [111]-oriented grains results in the smaller elongation along the out-of-plane direction than the theoretical value because the other type of grains elongate more than the theoretical value due to their higher compliance along those directions.

Next, the defect (mainly oxygen vacancy) concentrations of each type of grain are considered. Various thin films processing techniques of oxide films usually induce oxygen vacancy generation for various reasons. In the sputtering process of BST films, the low oxygen partial pressure and shot-peening effect generally induce high oxygen vacancy concentration. The average oxygen vacancy concentration, therefore, must be specifically determined by the adopted process conditions. However, due to the oxygen vacancy being generally low in density, it is often difficult to measure them by available spectroscopic means. In addition, it has not been feasible to estimate the oxygen vacancy concentrations in each type of grain in poly-crystalline oxide films. However, the accurate determination of the lattice parameters for each type of grain makes this possible as shown below. This is based on the work by Kim et al. where the lattice parameters of oxygen-deficient bulk BST material is reported to be determined by the oxygen vacancy concentration, which was controlled by the equilibrium oxygen partial pressure during annealing, for the given cation composition. One possible problem in applying the same method to the thin films, as in this work, is to achieve an unstrained lattice parameter \( a_0 \) for the differently oriented grains, which are free from the influence of any strain. This becomes possible by adopting the sin\(^2\)\(\psi\) method again. Details for the determination of \( a_0 \) using the sin\(^2\)\(\psi\) method were also, and the calculated sin\(^2\)\(\psi\) values for each type of grain for the cases of Ba/Sr ratios of 48/52 and 47/53 are included in the Table S IV of on-line supporting information.

Figure 4 shows the variation in the measured \( a_0 \) of the differently oriented BST grains as well as the Pt as a function of \( T_s \). There are three notable findings; first, they are generally much larger than the bulk lattice parameter with the same cation composition \( a_0 \) of bulk Ba$_{0.5}$Sr$_{0.5}$TiO$_3$ is 0.3947 nm, being indicated by a dashed line in Fig. 4. Second, the \( a_0 \) for each type of grain generally decreases with the increasing \( T_s \) having a different decreasing rate. Third, the \( a_0 \) for each type of grain are not the same. At \( T_s = 338 ^\circ C \) the difference is quite small. The largest \( a_0 \) was achieved from the [111]-oriented grains but the difference with \( a_0 \) of [002]-oriented grains, which is the smallest, is only ~ 0.002 nm. (See Table S V of on-line supporting information for the detailed numbers of \( a_0 \).) As \( T_s \) increases, the \( a_0 \) of the [111]-oriented grains decreases more significantly than the others and it becomes the smallest when \( T_s \) is > 400 °C. In addition, the difference with the other types of grains becomes larger as \( T_s \) increases. At \( T_s = 402 ^\circ C \), the \( a_0 \) of [110]-oriented grains is the largest but that of [002]-oriented grains becomes larger at 505 °C. Overall, the difference between the [002]- and [110]-oriented grains are generally smaller than that with [111]-oriented grains. It needs to be stressed that these lattice parameters are not influenced by the in- and out-of-plane strains.

The larger \( a_0 \) values for the various types of grains in BST thin film correspond to the higher oxygen vacancy concentration. The estimated identical \( a_0 \) of the Pt electrode to that of the bulk Pt material (down triangle symbol in Fig. 4) irrespective of the processing conditions suggests that other effects, such as strain and sputtering damage, can hardly influence the unstrained lattice parameters of the materials in the system. The different \( a_0 \) values of the BST grains with different orientations suggest that the oxygen vacancy concentration is also different. According to the results given by Kim et al. the oxygen vacancy concentration for the lattice parameters of 0.4020 nm is three times larger than that of 0.3970 nm. (It must be noted that the absolute values of the oxygen vacancy concentration cannot be compared but only relative values can be estimated in this way.) In other words, the different oxygen vacancy concentrations in different types of grains result in the different \( a_0 \) values even when all the grains were formed simultaneously under the given sputtering conditions. In general, the larger \( a_0 \) values compared to the bulk value of all cases suggest that all the films are generally oxygen deficient by the knock out effect from the energetic particle bombardments during the sputtering.

![Figure 4 | Variation in the measured unstrained lattice parameter, a0, of the differently oriented (Ba,Sr)TiO3 grains as well as the Pt as a function of substrate temperature. Dashed line indicates the bulk value of (Ba,Sr)TiO3.](www.nature.com/scientificreports)
The different variations in $a_0$ for the three types of grains with increasing $T_s$ are understood as follows. The almost identical $a_0$ at the $T_s$ of 338°C suggests that the vacancy concentration is dominantly determined by the knocking out effect during the sputtering process, which must be identical for all the three types of grains. The surface of the BST film was quite smooth demonstrating a highly uniform grain size irrespective of the types of grain due to the relatively incomplete crystallization at this low $T_s$ (See Fig. S 2b of on-line supporting information). It can be also understood that the in-plane compressive stress does not influence the vacancy concentration since the three types of grains have different levels of strains (Fig. 2). As the $T_s$ increases, the thermal healing effect appears to work and the vacancy concentration generally decreases. The larger decrease in the vacancy concentration for the [111]-oriented grains compared to the other two cases cannot be explained by the in-plane tensile stress effect, although this can be thought to be the case because the transition into the in-plane tensile stress state already occurs at $\sim 400^\circ$C for this case while the other two types of grains still remain in the in-plane compressive state up to $\sim 460$°C. This can be understood from the fact that the positive strain of the [111]-oriented grains is the lowest among the three but the vacancy concentration was the lowest (smallest $a_0$) for this case at the $T_s$ of 505°C. In fact, given the finding that the negative in-plane strain does not invoke any difference in the vacancy concentration between the different types of grains (338°C), it may not be reasonable to consider that the tensile stress induces the difference. Therefore, there must be some other factors, which influence the degree of oxygen vacancy healing depending on the types of grains.

It has been reported that the in-situ well-crystallized polycrystalline SrTiO$_3$, BaTiO$_3$ (BTO), and BST films tend to have roughened surface morphology due to the different growth habit planes of each grain$^{30}$. Hwang et al. reported that the [111]-oriented grains of BTO on the highly [111]-oriented Pt thin film electrode grows only on the vicinal planes of the [111]-oriented Pt grains while the [002]- and [110]-oriented grains grow on the (111) plane of the Pt grains$^{38}$. They invoked different surface charges and surface energies of the BTO materials depending on the types of crystallographic surfaces for such peculiar behavior of (local) epitaxial growth for such ionic oxide (BTO) on the metal (Pt) surface although the lattice mismatch is generally favorable for the usual epitaxial growth. Furthermore, the emergence of the three types of grains in this work is also believed to be due to such surface and interface-charge related arguments. As a result, the [002]- and [110]-oriented BST grains tend to have a flat surface as they may grow on the flat surface region of the [111]-oriented Pt grains, while the [111]-oriented BST grains tend to grow on the vicinal area of the Pt grains, which eventually results in the larger specific surface area of the [111]-oriented grains compared to the other two types of grain. (See Fig. S2 of the Supporting Information for TEM and atomic force microscopy (AFM)) Although this cannot be directly confirmed due to the lack of crystallographic information in the AFM images, the relatively rough surface morphology of the Pt electrode and several protruded grain shapes of BST films revealed by AFM (Fig. S2 of on-line supporting information) revealed that the specific surface area of the [111]-oriented BST grains is larger than those of the two others. TEM also confirmed this (See Fig. S2 of on-line supporting information). The larger surface energy of (111) planes also contribute to the suppression of the flat (111) surface in [111]-oriented BST grains. With this assumption, the faster healing effect of the [111]-oriented grains can be understood; the larger surface area of this type of grain enhances the vacancy annihilation during the growth at a higher $T_s$. At lower $T_s$, the generally less evident evolution of grain morphology of the different grains makes this difference less evident and thus the vacancy healing effect must be averaged out.

Up to now, the influences of $T_s$ on the evolution of strain and oxygen vacancy concentration for each type of BST grains have been discussed. Next, the effects of film thickness ($t_f$) on the evolution of the strains will be discussed for the films grown at 505°C. $t_f$ was varied from 29.6 nm to 155.8 nm, and the detailed information of these films, such as the $\Theta$ XRD data and cation composition are included in the on-line supporting information (Figures S4 and S5). All the films showed identical crystallographic growth behavior and cation compositions irrespective of the $t_f$ within the experimental error ($\sim 1$ at. %).

The in- and out-of-plane strains of the [111]-, [110]-, and [002]-oriented grains are also examined by the sin$^2\psi$ method, and the variations in the lattice parameters of Pt electrode films, [111]-, [110]-, and [002]-oriented BST grains, respectively, as a function of sin$^2\psi$ for the BST films with different $t_f$ are included in Fig. S6 of the Supporting Information. The results for the BST grains are summarized in Fig. 5. Figures 5a-c show the variations in the $\varepsilon_1$ and $\varepsilon_2$ values as a function of the $t_f$ for the three differently oriented grains. The $\varepsilon_1$ and $\varepsilon_2$ values generally decrease with the increasing $t_f$. However, the overall difference between the different types of grains is quite identical to that shown in Fig. 2; the strain of [002]-oriented grains is symmetrical and largest while that of [111]-oriented grains is asymmetrical and smallest. Table II shows the same comparison between the calculated and measured $\nu$ values of the three types of grains at two representative $t_f$. The experimental $\nu$ of the other $t_f$ films are exactly the same as those shown in Table II. A same tendency as that in Table I can be found.

Figure 5d shows the variations of unstrained lattice parameter ($a_0$) for the different types of grains as a function of $t_f$. Bulk $a_0$ value (0.3947 nm) of the (Ba$_{0.5}$Sr$_{0.5}$)TiO$_3$ is indicated by dashed line in the figure. The $a_0$ for each type of grain is almost independent of the $t_f$ but only depends on the type of the grain. This means that the overall oxygen vacancy concentration is not dependent on $t_f$ while the strain is dependent on it. Moreover, this suggests that the strain relaxations shown in Fig. 5a-c are not due to healing out of the oxygen vacancies or agglomeration of the oxygen vacancies to form the dislocations. Conversely, this also coincides with the fact that the film stress hardly has an influence on the vacancy concentration, as discussed above.

**Discussion**

In this work, the strain state of in-situ crystallized poly-crystalline BST thin films on Pt electrodes were carefully examined using the sin$^2\psi$ method in the X-ray diffraction technique. The poly-crystalline BST thin films deposited at substrate temperatures ranging from 338 to 505°C showed a relatively random orientation with [002]-, [110]-, and [111]-oriented grains along the normal direction to the surface, of which strain states are different although they were grown simultaneously. In addition, the transition temperature where the strain state of each grain changes from the in-plane compressive state, which is believed to be due to the shot-peeking effect of the sputtering process, to the in-plane tensile state, which is due to the thermal expansion mismatch between the BST film and substrate, was also different. This is a highly unexpected result as opposed to the general conjecture that the every grain in poly-crystalline film has an identical strain (and stress, too) under the given growth conditions due to the strong mechanical confinement between the neighboring grains. The different compliances along the out-of-plane direction of the different types of grains resulted in the different strains responding to the external in-plane stress.

The unstrained lattice parameter, which is dominantly governed by the oxygen vacancy concentration for each type of grain, was also different suggesting the vacancy concentration is different. Interestingly, such a discrepancy has no correlation with the different strain state for each type of grain but appeared to be related with the specific surface area, which provides the grains with oxygen atoms at higher growth temperatures.

The trends of the orientation-specific strain state was maintained in a wide thickness range (29.6 $\sim$ 155.8 nm) although thicker films
After the Si substrate was cleaned, 100-nm-thick SiO₂ was thermally grown and

**Methods**

Methods

After the Si substrate was cleaned, 100-nm-thick SiO₂ was thermally grown and 10-nm-thick amorphous Al₂O₃ layer was deposited by an atomic-layer-deposition process in order to improve the adhesion between the substrate and the Pt electrode that was deposited on top by a dc sputtering technique. The Pt electrode thickness was 100 nm and had a highly [111] preferred growth behavior in the out-of-plane direction while the crystallographic direction in the in-plane direction is completely random. BST films with thicknesses ranging from 29.6 to 155.8 nm were deposited by an rf sputtering technique using a ceramic target under a sputtering pressure of 10 mTorr (O₂/Ar gas ratio = 10%). The substrate temperature was varied from 338 to 505°C. 338°C was just enough Tₛ to grow the in-situ crystallized poly-crystalline BST film. Film cation composition ratios, [Ti]/[Ba + Sr + Ti] and [Ba]/[Ba + Sr], were estimated by X-ray fluorescence spectroscopy (See on-line supporting information). X-ray diffraction was performed using a Cu kα radiation, which was monochromatized by a curved graphite monochromator. A Hybrid Mirror type X-ray detector was used to enhance the resolution and minimize the measurement error and analysis time. The Θ–2Θ scan was used to determine the crystallographic orientation of the film. The sin² ϑ method was used in order to detect the strain and unstained lattice parameter of each grain. Lastly, the X-ray pole figure measurement was also used to determine the degree of randomness of the in-plane crystallographic direction for each type of grain.

The microstructure of the film was observed using high-resolution transmission electron microscopy (HRTEM) and atomic force microscopy (AFM) (See on-line supporting information).

**Table II | Comparison between the calculated and experimental Poisson’s ratio for the cases of 29.6-nm- and 155.8-nm-thick (Ba,Sr)TiO₃ films grown at 505°C**

|  | calc. (10⁻¹² m²/N) | calc. | meas. (at 29.6 nm) | meas. (155.8 nm) |
|---|---|---|---|---|
| ζ₀/ζ₀ | 0.047 | 0.850 | 0.942 | 0.942 |
| ζ₂/ζ₀ | 3.240 | 0.563 | 0.454 | 0.454 |
| ζ₃/ζ₀ | 2.971 | 0.433 | 0.342 | 0.342 |

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**Author contributions**

W.Y.P. performed the deposition and X-ray experiments, and analyzed the data; M.H.P. analyzed HRTEM and AFM images, and wrote the paper partly; J.H.L. performed HRTEM analysis; J.H.Y. performed AFM analysis.; J.H.H. wrote the paper partly; J.H.C. and C.S.H. designed the experiments, and wrote the paper.

**Additional information**

Supplementary information accompanies this paper at http://www.nature.com/scientificreports

Competing financial interests: The authors declare no competing financial interests.

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