Bacterial Hash Function Using DNA-Based XOR Logic Reveals Unexpected Behavior of the LuxR Promoter

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SYNOPSIS

Introduction: Hash functions are computer algorithms that protect information and secure transactions. In response to the NIST’s “International Call for Hash Function”, we developed a biological hash function using the computing capabilities of bacteria. We designed a DNA-based XOR logic gate that allows bacterial colonies arranged in a series on an agar plate to perform hash function calculations.

Results and Discussion: In order to provide each colony with adequate time to process inputs and perform XOR logic, we designed and successfully demonstrated a system for time-delayed bacterial growth. Our system is based on the diffusion of β-lactamase, resulting in destruction of ampicillin. Our DNA-based XOR logic gate design is based on the opposition of two promoters. Our results showed that Plux and PompC functioned as expected individually, but Plux did not behave as expected in the XOR construct. Our data showed that, contrary to literature reports, the Plux promoter is bidirectional. In the absence of the 3OC6 inducer, the LuxR activator can bind to the Plux promoter and induce backwards transcription.

Conclusion and Prospects: Our system of time delayed bacterial growth allows for the successive processing of a bacterial hash function, and is expected to have utility in other synthetic biology applications. While testing our DNA-based XOR logic gate, we uncovered a novel function of Plux. In the absence of autoinducer 3OC6, LuxR binds to Plux and activates backwards transcription. This result advances basic research and has important implications for the widespread use of the Plux promoter.

Keywords: hash function, time-delayed bacterial growth, DNA-based XOR logic gate, Plux, LuxR, PompC, bidirectional promoter, synthetic biology
Reports on negative result

Introduction

Protection of electronic communication is vital to the economic and defense capabilities of our nation. “America’s Next Top Hash Function” competition, as Wired Magazine describes it, recognized the need for a novel hash function in light of recent attacks on the integrity of the current standard and challenged the global community to design a secure hash function standard. In late 2012, the U.S. National Institute of Standards and Technology (NIST) will conclude their international competition for the development of a new and improved hash function and a winner will be chosen from five finalists. The competition was introduced in November 2007 in response to concerns that the current standard, SHA-1 (Secure Hash Algorithm) was out-of-date and not secure. A secure cryptographic hash algorithm is essential to authenticate electronic documents and maintain their integrity. Hash functions also protect passwords, software, and monetary transactions from hackers. A hash function encrypts an input of arbitrary length into a “message digestion” code of fixed small size in a way that is irreversible, meaning the input cannot be deduced from the output. The hash output value of a given input string is its “signature” or “fingerprint” that works to detect document tampering. The ideal hash function must satisfy three properties: preimage resistance, second preimage resistance, and collision resistance. Preimage resistance refers to the difficulty of finding an input that hashes to a pre-specified output. Second preimage resistance describes the difficulty of identifying a second input that hashes the same output as a given input. Collision resistance is a measure of the likelihood that the same hash value is produced by two distinct inputs. A good hash function is completely irreversible and designed so that collisions are as rare as possible. In addition, it should be quick and easy to extract an output from a given input message.

In response to the call for a reliable and novel hash function, we developed a biological hash function to be implemented inside living bacteria. Bacterial computers provide a unique alternative technology to silicon computers. Cellular computers have the advantage of exhibiting enormous parallel computing capabilities, intercellular communication, ability to interface with the biological world, and reusability. Computing efficiency may result from the use of single analog logic gates in a population of bacterial computers, as opposed to the thousands of gates required in digital processes used by conventional computers. Furthermore, computer hackers are untrained in decoding biological computers. We chose the XOR (exclusive OR) logic gate to execute our biological hash function. Among the basic Boolean logic operators, only the XOR and NXOR gates possess an equal chance for an output of 0 or 1. In an XOR logic gate, an output is produced if and only if exactly one of the binary inputs is present. If both inputs are present, or both inputs are absent, the logic gate does not produce an output.

As a proof-of-concept, we designed a simple linear hash function out of a sequential series of bacterial colonies, each of which performs XOR logic on inputs consisting of one bit from the message and one bit from the output of the previous colony. In addition to this simple linear model, we designed several more complex, three dimensional, and detailed alternative hash functions. As shown in Figure 1, the first colony uses XOR logic to respond to two chemical inputs, one in the form of a key and the other as the first part of the input message. The output from the first colony is used as input for the second colony, along with the next bit of the input message. These two inputs are processed by XOR logic in the second colony and the output is passed on to each successive colony in the series. The final colony output determines the hash value of the input “message”.

Encoding an XOR logic gate in a biological system necessitates that a cell differentially respond to an input depending on whether the input is presented alone or in combination with another input. Differential response to an input presents a formidable challenge, which explains why engineering of a direct DNA-based XOR gate has not been reported. The assembly of a chemistry-based XOR logic gate has been reported, with amines and protons as inputs.

Voigt, et al. (2011) recently assembled an indirect DNA-based XOR gate but only through a combinatorial circuit consisting of three NOR gates, a buffer gate, and a specific spatial arrangement on the agar plate. Stojevic, et al. (2002) designed an in vitro “deoxyribozyme-based” XOR gate consisting of single-stranded oligonucleotides of switched loops acting as inputs and cleaved oligonucleotide products as the output. In contrast to XOR gates, researchers have been able to successfully construct and implement other DNA-based Boolean logic gates in vivo, including AND, OR, NOT, NOR and NAND logic.

Our goal was to design and test a direct DNA-based XOR logic gate that could be used in a series of bacterial colonies to implement a hash function. XOR logic requires that the presence of two inputs produces no output (Figure 2). In order to accomplish this result in a biological system, we selected two inducible promoters to be placed in opposition to one another. When both promoters are induced, transcription would be blocked by the binding of their respective DNA-binding proteins and RNA polymerases. One of the promoters is the P_{lux} promoter, a well-documented and widely used synthetic biology part from the LuxR quorum sensing mechanism. One of the first quorum sensing systems discovered, the luxR operon was isolated from V. fisheri, a marine bacterium living symbiotically within the squid Euprymna scolopes. According to the literature, the transcriptional activator protein LuxR must first bind to its ligand, the chemical autoinducer 3-oxo-C_{12}-homoserine lactone (3OC6), before LuxR can bind to, and subsequently activate, the promoter P_{lux}. The autoinducer 3OC6 is synthesized by the bacterially encoded LuxI enzyme. Once P_{lux} is activated, the luxI gene is transcribed at a high rate, initiating a positive feedback autoinduction circuit. For the opposing promoter, we utilized the ompC/envZ signaling system. P_{ompC} is part of the endogenous osmotic stress response.
response unit in *E. coli* that becomes activated in media of high osmolarity. Wild-type *E. coli* cells possess the outer membrane pore proteins, OmpF and OmpC, that are reciprocally regulated by the osmolarity of their surrounding environment. In high osmolarity media made with the addition of NaCl, such as LB, OmpC is transcribed and cells accumulate the smaller OmpC passive diffusion pores in their membranes. In low osmolarity media, such as TY, *ompF* encodes a large diameter pore. A histidine kinase protein, EnvZ, monitors osmolarity in the vicinity of the cell and phosphorylates a transcription factor, OmpR, and phospho-OmpR promotes transcription of *ompC* via its *P*ompC promotor.

In the context of the XOR gate, the addition of 3OC6 to the media serves as one input while the addition of NaCl (high osmolarity LB media) serves as the other input. When both inputs are present or when both are absent, the logic gate is predicted to return no output. The XOR gate will be encoded into each of the colonies depicted in Figure 1. The hash function key will take the form of the presence or absence of 3OC6 and will be one of the two inputs to the XOR function of the first colony. The other input will be the presence or absence of NaCl administered adjacent to the first colony, representing the first part of the message. The first colony will process these two inputs and deliver an output in the form of the presence or absence of 3OC6 to the second colony. The second XOR input for this colony will be the presence or absence of NaCl administered adjacent to the second colony, representing the second part of the message. In this way, successive colonies will process the message, with the output from the previous colony as the presence or absence of 3OC6 connected to the expression of a reporter gene such as RFP in the final colony.

The design of our DNA-based XOR gate was based on an understanding of the molecular mechanisms by which the two promotors function, as documented in the literature. The two promotors functioned as expected when tested individually, but we detected aberrant behavior when testing the complete XOR configuration with opposing promoters. Frequently in synthetic biology, devices function as designed and the project is deemed successful. However, synthetic biology devices occasionally fail due to incomplete understanding about parts that are central to the design. It is important that synthetic biologists learn to investigate the reasons for failed designs in the interest of basic research and the purpose of redesign. In this case, we discovered that the transcription factor LuxR and the *P*lux promoter do not function as previously reported.

This result contributes to basic research that complements our successful demonstration of time-delayed bacterial growth, which is a contribution to applied research.

**Results and Discussion**

In order for the XOR-based hash function to process information over time, each colony in the series must perform its logic sequentially. If all colonies grew simultaneously, the hash function would fail because colonies at the end of the chain would perform their XOR logic before the input from the previous colony had reached them. Thus, we needed to devise a mechanism of time-delayed growth so that colonies would sequentially process their inputs and pass along their output to the next colony before the following colony had grown and performed XOR logic. A literature search failed to uncover a technique to accomplish time-delayed growth in a simple and inexpensive way. We took advantage of the often unintended consequence of satellite colonies forming when transformed colonies are left on an ampicillin selection plate too long. Following a bacterial cell transformation, satellite colonies can form around resistant colonies containing cells that successfully integrated an ampicillin-resistance plasmid. Ampicillin is often mistakenly thought to kill *E. coli* outright but ampicillin and other β-lactams prevent cell wall peptidoglycan synthesis by the competitive inhibition of a transpeptidase, thereby preventing the bacteria from forming new cell walls during cell division. Ampicillin-resistant cells can secrete up to 90% of the enzyme β-lactamase beyond the periplasmic space when the enzyme is highly expressed. The enzyme cleaves the β-lactam ring of ampicillin and inactivates the antibiotic. Non-ampicillin-resistant satellite colonies grow because ampicillin is deactivated surrounding the β-lactamase secreting cells and viable ampicillin-sensitive cells can thrive once again after hours of no growth. We exploited this often undesirable artifact to produce time-delayed colony growth. Previous research suggested that β-lactamase diffuses slowly through LB agar, thus providing a means to control the growth of colonies in a time-dependent manner. We successfully demonstrated time-delayed growth produced by β-lactamase diffusion (Figure 3). An inoculant of ampicillin-resistant bacteria was placed at one edge of an agar plate with ampicillin-sensitive bacteria inoculated every 0.5 cm along a line in each of three directions. As the β-lactamase secreted by the ampicillin-resistant bacteria diffused across the plate, ampicillin-sensitive bacteria at increasing distances from the ampicillin-resistant bacteria were able to grow. The spread of colonies over time indicates...
that β-lactamase was conferring ampicillin-resistance to colonies sequentially and uni-directionally. (A video of this time-delay growth can be accessed online).

Time-delayed growth could allow for temporal tuning of a bacterial hash function since successive colonies would be given adequate time to process their XOR logic. We characterized our time-delayed colony growth system further and investigated what variables could be manipulated to govern the rate of colony growth. We measured the rate of ampicillin inactivation as a function of three variables: initial ampicillin concentration, agar concentration, and temperature (Figure 4). Over the course of three days, the appearance of colonies was linear. Ampicillin-sensitive colonies appeared faster with lower concentrations of ampicillin, as expected (Figure 4A). We hypothesized that higher agar concentrations would slow the diffusion of β-lactamase across the plate and therefore slow the ability of colonies to grow. Contrary to our expectations, higher agar concentration produced faster colony appearances (Figure 4B). Temperature also had an interesting effect on the appearance of non-resistant colonies. At a high concentration of ampicillin (100 µg/mL), there was no significant difference in the rate of delayed growth between the 30°C and 37°C (compare Figures 4A and 4C). However, at a lower ampicillin concentration (25 µg/mL), appearance of colonies was 1.5 times faster at 37°C (compare Figures 4A and 4C).

To test the function of our proposed XOR-based hash function, we built the construct depicted in Figure 2A. By arranging the promoters of the OmpR and LuxR signaling system head-to-head and coupling each to a distinct fluorescent protein marker, we could determine if XOR logic was processed inside live E. coli cells (Figure 2B). When cells are grown in high salt LB media and without the addition of 3OC6, P0mpc should be activated and cells should fluoresce green. When 3OC6 is added to a low salt TY media, Plux should be activated and cells producing LuxR should fluoresce red. When cells are grown in low salt TY media in the absence of 3OC6 or in high salt LB media in the presence of 3OC6, cells should not fluoresce at all.

Figure 5A shows the results of experiments to test the function of the XOR gate. We measured RFP and GFP fluorescence under all four combinations of inputs in the presence of the LuxR regulatory protein. In the absence of LuxR, we expected that the Plux promoter would not function (Figure 5B). No expression of the RFP gene is expected, and none was observed. We predicted that the absence of LuxR would have no effect on the ability of P0mpc to respond to the high osmolarity input of NaCl in the LB media and that is what we observed. The observation of GFP expression when both the 3OC6 and high osmolarity inputs were provided was consistent with the explanation that LuxR was not available to activate transcription form the Plux promoter. In the presence of the LuxR regulatory protein and absence of both inputs, we observed unexpected GFP expression. In the presence of LuxR and the 3OC6 input combined with the absence of the high osmolarity NaCl input, we observed RFP expression as predicted. The result of GFP expression in the presence of high osmolarity NaCl input and the absence of the 3OC6 input was also in accord with our expectations. When both inputs were present, we observed lower levels of unpredicted GFP expression. The presence or absence of both inputs proved to be the conditions that produced the unexpected behaviors when LuxR was expressed inside the cells.

In order to explain the unexpected behaviors of GFP expression, we hypothesized that the Plux promoter was stimulating backward transcription in the presence of LuxR but the absence of the 3OC6 autoinducer. The results of experiments to test this hypothesis are shown in Figure 5C. The test construct was designed to result in RFP expression only when backwards transcription is supported by the BioBrick part containing the Plux promoter. In the absence of LuxR, the addition of 3OC6 did not result in backwards transcription. However, the same construct, with the addition of the LuxR protein, had a very similar level of fluorescence with or without the addition of 3OC6. Although there is less transcription of RFP in the presence of 3OC6 than in the absence of 3OC6, the differences are not significant. Perhaps the lower average and larger error bars is due to stochastic binding of 3OC6 and the resulting inconsistent forward vs. backward transcription from the same promoter. The literature indicates that LuxR binds Plux only after 3OC6 binds to LuxR14, 15 24-26. Our results show that the BioBrick part containing Plux supports backwards transcription when LuxR is present in the cell and 3OC6 is absent. The backwards transcription from Plux in the presence of LuxR also explains the failure of the XOR gate to perform its logical operations. It is worth noting that the Plux promoter used in this study contains only the -10 and -35 regions with a lux box but not the additional 70 bp portion of DNA found in V. fischeri that normally leads to the transcription of LuxR24.

Conclusion and Prospects

Our design of a biological hash function using a direct DNA-based XOR logic gate was a novel response to the international call for a new and improved standard hash function17. Our bacterial hash function provided a new approach for a robust and secure

![Figure 4. Bacterial growth rate. A) The effect of ampicillin concentration on growth rate in time-delayed growth at 37°C. B) Effect of agar concentration on bacterial growth rate at 37°C. Media are described by agar concentration (0.5x = 7.75 g/L) over ampicillin concentration (25 = 25 µg/mL). C) The effect of ampicillin concentration on bacterial growth rate at 30°C. Error bars in all three panels are standard error of the mean, though many are smaller than the data point shapes.](image_url)
coding system inside live cells compared to current hash functions based on complex hardware and algorithms. For certain applications, biological computation is superior to *in silico* computation because populations of cells can execute vast amounts of processes in parallel relatively inexpensively, and because of the cell's natural connection to the living world. For our bacterial hash function, we chose to implement an XOR logic gate because it integrates two inputs and provides equal distribution of outputs\(^5\). In addition to a potential hash function, biological logic gates have been studied for various other purposes and could be extremely useful in agriculture, production of pharmaceuticals and other products, and in medicine, particularly in the detection of cancer cells\(^\text{16}\).

In order to implement a simple hash function with a series of XOR logic gates, we designed and successfully demonstrated time-delayed growth of bacterial colonies based on the characteristic diffusion of β-lactamase in agar. Time-delayed bacterial growth ensures that each colony would be given sufficient time to unidirectionally process its inputs and perform XOR logic sequentially so that the message would be correctly hashed. An inexpensive and simple procedure for time-delayed growth could be a valuable tool for synthetic biologists who need signals to be passed to neighboring cells over a defined time period. As expected, we saw that bacterial growth rate decreased with a greater concentration of ampicillin. We incorrectly hypothesized that increased agar concentration would decrease bacterial growth rate because it would slow the diffusion of β-lactamase. After performing a literature search, we found that naficillin, which is structurally similar to ampicillin, is less effective when agar concentration is high\(^\text{85}\). Sequestration of the antibiotic by agar would explain the increased bacterial growth rate we observed. The observation of a higher bacterial growth rate at higher temperature for the 25 µg/mL ampicillin concentration suggests that β-lactamase enzyme function or diffusion is increased with temperature. Further studies should measure the effects of a wider range of temperatures and ampicillin concentration to understand the interaction between the two variables. Given that over production of β-lactamase enhances its own secretion\(^\text{87}\), it would be informative to test the effect of plasmid copy-number on sequential bacterial growth, which could present an additional method of tuning the growth rate of bacteria. In one study, researchers found that employing low-copy plasmids and adding selective pressures with an antibiotic resistant gene significantly attenuated internal noise in gene circuits\(^\text{32}\). While we investigated the basic effects of initial ampicillin concentration, agar concentration, and temperature, further characterization is required to be able to fully develop and take advantage of time-delayed colony growth.

Our XOR logic gate was based on the opposition of the P\(_{\text{ompC}}\) and P\(_{\text{lux}}\) promoters. The designed logic gate did not function as predicted because of previously undocumented behavior of the BioBrick part containing the P\(_{\text{lux}}\) promoter. In future studies, we would need to replace the P\(_{\text{lux}}\) part with one that contains a unidirectional promoter that becomes activated only in the presence of its input signal. Candidate promoters include P\(_{\text{luxR}}\), P\(_{\text{lux}}\), and P\(_{\text{lux}}\) which have been studied for use in other biological logic gates\(^\text{14,24}\).

Our results indicated that the P\(_{\text{lux}}\) promoter is bidirectional and is induced "backwards" by LuxR in the absence of 3OC6. The backwards transcription in the absence of 3OC6 had not been documented in the literature\(^\text{14,15,24}\). In the *V. fischeri* genome, the P\(_{\text{luxR}}\) promoter points in the direction of the LuxG gene and away from the LuxR gene. The native luxR gene has its own promoter “pointed to the left” but low levels of backwards transcription is possible from the adjacent P\(_{\text{lux}}\) promoter “pointed to the right”\(^\text{21}\). In these experiments, LuxR was produced by “backwards transcription” in the presence of LuxR and 3OC6 but not with LuxR alone. The experiments that showed “backwards” promoter activity was 3OC6-dependent used the full P\(_{\text{lux}}\) promoter that includes 70 additional bases compared to the P\(_{\text{lux}}\) used in this study. In our experiments, the level of backwards transcription by P\(_{\text{lux}}\) in the presence of LuxR alone was greater than that of forwards transcription from P\(_{\text{lux}}\) in the presence of both LuxR and the inducer 3OC6.

The current study suggests that in the absence of 3OC6, transcription in the direction of LuxR might also produce a positive feedback loop for LuxR production\(^\text{17}\). Backwards transcription from the P\(_{\text{lux}}\) promoter could be caused by attachment of LuxR to known binding sites in P\(_{\text{lux}}\). Alternatively, there could be a cryptic promoter in the P\(_{\text{lux}}\) part that contains additional LuxR binding sites that have not yet been studied. The behavior of the LuxR regulatory protein may also be due to cytoplasmic differences between its native *V. fischeri* bacterial cells and *E. coli* cells. The LuxR family of quorum-sensing proteins includes hundreds of orthologs across many species of prokaryotes. In nature, *E. coli* bacteria express a signal receptor in this family known as SdiA but do not possess an orthologous enzyme (such as LuxI) that produces signals (such as 3OC6 and other N-acylhomoserine lactones[AHL]). Instead, *E. coli* is thought to detect and respond to the signals produced by other neighboring species, but this has been difficult to study\(^\text{27}\). A recent study by Dyszel, et al. (2010) demonstrated that sdiA is only partially dependent on AHL because plasmid-based sdiA induced a response in two important loci of *E. coli*, but not chromosome-based sdiA and/or AHL\(^\text{83}\). More research is necessary to investigate the mechanism of AHL detection in *E. coli*. Since the LuxR we transformed into *E. coli* was plasmid-based, the similarity to plasmid-based sdiA might influence the unpredicted behavior of P\(_{\text{lux}}\). Perhaps P\(_{\text{lux}}\) should not be thought of as initiating “backwards” tran-
scription, but $P_{ux}$ with LuxR should be described as a toggle switch that is governed by the presence or absence of 3OC6. In our experiments, the level of backwards transcription by $P_{ux}$ in the presence of LuxR alone was greater than that of forwards transcription from $P_{ux}$ in the presence of both LuxR and the inducer 3OC6.

We have made progress towards a functional bacterial hash function with the development and testing of a novel design. We developed and characterized a method for inexpensive and simple time-delayed growth that is necessary for implementation of our hash function and is likely to find general utility in synthetic biology. Our DNA-based XOR logic gate did not function as expected, so we designed and built control constructs that provided data in support of more complete description of the molecular mechanism by which the LuxR activator controls bidirectional transcription from the commonly used $P_{ux}$ promoter.

Materials and Methods

Bacterial growth

For measurement of time-delayed bacterial growth, LB agar plates were prepared by dissolving 1 g Bacto-tryptone, 5g yeast extract, 10g NaCl in 800 mL water, adjusting the pH to 7.5 with NaOH, adding agar, and adjusting the final volume to 1 L. Agar added at a level of 7.5g was designated 0.5 X, while 15g was 1.0 X, and 22.5g was 1.5 X. After sterilization, ampicillin was added to final concentrations of 25 µg/mL, 50 µg/mL, or 100 µg/mL. Each plate was inoculated in one corner with 2 µL of an overnight culture of an ampicillin-resistant strain of $E. coli$. 2 µL of ampicillin-sensitive JM109 $E. coli$ overnight culture were inoculated. Plates were incubated at either 30°C or 37°C for still/video photodocumentation or measurement of the average distance to the farthest visible colony.

Testing of $P_{ux}$ used low and high osmolarity liquid media. LB media was prepared with 10g of tryptone, 5g of yeast extract, 5g NaCl and 200 µL of 5 M NaOH per liter of distilled water. TY liquid media was prepared with 10g of tryptone and 5g of yeast extract and no NaCl per liter of distilled water[48]. LB media was considered to be high osmolarity by comparison to the low osmolarity of the TY media, prepared without addition of NaCl. Ampicillin was added to a final concentration of 100 µg/mL. Testing of $P_{ux}$ required the autoclave 3OC6-HSL (Sigma-Aldrich Cat. # K3007), added to a final concentration of 4 µg/mL.

Basic BioBrick assembly

All DNA parts and sub-parts produced for this project were generated using the standard BioBrick assembly protocol using high copy plasmids pSB1AK3, pSB1A2 or pSB1A3[34], and registered on the MIT Registry of Standard Biological Parts[36]. The Promega Wizard Plus SV Miniprep (Cat. #A1460) kit was used according to the manufacturer’s instructions to extract plasmid DNA. BioBrick parts were digested with restriction enzymes, EcoRI, XbaI, SpeI, and PstI to produce ‘sticky ends’ that were used to combine BioBrick parts. Digests were purified using agarose gel electrophoresis followed by gel purification with the QIAGEN QiAquick Gel Extraction Kit (Cat. # 28706). BioBrick parts with matching ‘sticky ends’ were ligated using T4 ligase produced by Promega. Plasmid DNA was transformed into JM109 Z-Competent $E. coli$ cells (Zymo Research Cat. # T3003) according to the manufacturer’s instructions. It is important to note that JM109 cells express the LacI repressor, which inhibits pLac promoters[37]. Colonies from ligation reactions were screened by polymerase chain reaction (PCR). All PCR reactions in this project were performed using Promega GoTaq Green Master Mix (Cat. # M7123) with the appropriate primers and template DNA. All final constructs were sequenced for verification.

Construction of basic parts

The 99 base pair $P_{ux}$ promoter (K199017) was cloned from the MC4100 strain of $E. coli$ using polymerase chain reaction (PCR). Primers were synthesized by Eurofins MWG|Operon using an online PCR primer design program[46]. The forward primer has the sequence 5’ GCTAGATTCCGGCGCGTCTTAGGTTA CATTTCGAAACATCTA 3’. The underlined portion is a 20bp sequence that is the first 20bp of the $P_{ux}$ promoter[19]. The 5’ end of the primer is the standard BioBrick prefix[23], consisting of three different restriction sites, EcoRI, NotI and XbaI, plus four bases (GCAT) to facilitate EcoRI digestion at the 5’ end of the PCR product. The reverse primer has the sequence 5’ GCACTGCGACGGCG CGCTACGATGTTCCGGTTCCCGAAAAATG 3’. The underlined portion is a 21bp sequence that is complementary to the last 21bp of the $P_{ux}$ promoter[19]. The 5’ end of the primer consists of the complement of the restriction sites of SpeI, NotI and PstI to form the standard BioBrick suffix[19]. The four bases GCAT were added to the 5’ of the primer to facilitate PstI digestion on the 3’ end of the PCR product (BBa_K199017). PCR was conducted using MC4100 strain of $E. coli$ as a source of template. The PCR product was purified, ligated into a BioBrick vector, and transformed into JM109 cells. Putative clones were screened by DNA sequencing.

The 55 base pair $P_{ux}$ promoter (BBa_K199052), which includes the lux box[28], was required to be opposite in orientation relative to $P_{ux}$ in order to facilitate our XOR gate design (Figure 2). The $P_{ux}$ reverse promoter $P_{ux-rev}$ was generated by assembling four smaller oligos together. The sequences for the four oligos were generated using the online “Oligo Out” Optimization Program[45]. The oligos were modified so that the two ends of $P_{ux}$ were equivalent to BioBrick prefix and suffix that have been digested with EcoRI and PstI. The oligos were produced by Eurofins MWG|Operon. The sequences of the oligos were 5’ ATTTCGCGCGCGTTCTA GGTATTACGACTA 3’, 5’ TAACAAACCATTTTCTTCTTGGTAA ACC TGTAGCAGCTCTACAGTTGACAGTGCGCCGCGCTGCA 3’, 5’ TAC AGGTTTACGCAAGAAATGGTTGTATATCGAATTACCTGTA GAGCCGCGCCGCG 3’, and 5’ GCGGCCGCTAGCTTAACCTGTA GATCG 3’. For measurement of time-delayed bacterial growth, LB agar plates were prepared by dissolving 1 g Bacto-tryptone, 5g yeast extract, 10g NaCl and 200 µL of 5 M NaOH per liter of distilled water. TY liquid media was prepared with 10g of tryptone and 5g of yeast extract and no NaCl per liter of distilled water[48]. LB media was considered to be high osmolarity by comparison to the low osmolarity of the TY media, prepared without addition of NaCl. Ampicillin was added to a final concentration of 100 µg/mL. Testing of $P_{ux}$ required the autoclave 3OC6-HSL (Sigma-Aldrich Cat. # K3007), added to a final concentration of 4 µg/mL.

Construction of composite parts

The part RFP+rev+RBS$_{lux}$ (BBa_K199021) was formed by ligating the pre-existing parts, RFP$_{rev}$ (BBa_J31008) and RBS$_{lux}$ (BBa_J440 01). The parts RFP$_{rev}$, RBS$_{lux}$ and RBS+GFP (BBa_E5500) were ligated to $P_{ux}$ (BBa_R062) and $P_{ux}$ (K199017) so that two constructs, RFP$_{rev}$+RBS$_{lux}$+GFP (promoter) and (promoter)+RBS+GFP were built for each promoter, except for $P_{ux}$ +RBS+GFP which had been previously constructed (P$_{ux}$-BBa_K199019; BBa_K199022; P$_{ux}$-BBa_K199027). The purpose of the (promoter)+RBS+GFP constructs was to quantify the level of transcription in the direction the promoter is pointing, while the RFP$_{rev}$+RBS$_{lux}$+GFP (promoter) constructs was used to quantify the amount of transcription caused by each promoter in the reverse direction. Note that the pre-existing part (BBa_K90100) designed containing P$_{ux}$ +RBS+GFP also contained P$_{ux}$ +RBS+Lux+R-TT (TT is a transcription terminator) to the left of it because LuxR is required for $P_{ux}$ to be activated[35].

For the experiment measuring forward activity, the constructs tested were $P_{ux}$+RBS+GFP (BBa_K199019) and P$_{ux}$+RBS+ Lux+R-TT+P$_{ux}$+RBS+GFP+TT (BBa_K09100). BBa_K09100 was tested with and without IPTG and 3OC6-HSL. For the experiment
measuring backward activity, the constructs tested were RFP<sub>rev</sub>+RBS<sub>rev</sub>+P<sub>lac</sub> (BBa_K199022), RFP<sub>rev</sub>+RBS<sub>rev</sub>+P<sub>lac</sub> (BBa_K19902), and P<sub>rev</sub>+RBS+RFP (BBa_J04450) as a control.

For construction of the XOR logic gate, the construct RFP<sub>rev</sub>+RBS<sub>rev</sub>+P<sub>lac</sub> (BBa_K199022) was ligated to P<sub>rev</sub> (BBa_K199052) then to RBS+GFP (BBa_E5500) to make the construct RFP<sub>rev</sub>+RBS<sub>rev</sub>+P<sub>rev</sub>+RBS+GFP (BBa_K199069). LuxR expression with the XOR gate (BBa_K199104) was produced by ligating the XOR construct (BBa_K199069) to the right of P<sub>rev</sub>+RBS+LuxR+TT (BBa_K199103). LuxR production was induced when IPTG is added and activates P<sub>rev</sub><sup>+</sup>. However, it should be noted that P<sub>rev</sub> is known to be a leaky promoter with significant transcription activity even in the absence of IPTG<sup>17</sup>

Measuring fluorescence

For measurement of fluorescence, 2 mL of liquid media was inoculated with the appropriate cells and incubated for 18 hours at 37°C with shaking. After incubation, 600 µL of each construct-media combination was transferred to a microwell plate in 200 µL triplicates. The microwell plate was analyzed using a fluorometer to obtain an absorbance reading and a fluorescence intensity for each 200 µL sample. Each fluorescence intensity value was divided by its corresponding absorbance (959 nm) reading to account for the varying levels of growth in each culture tube. Triplicates were then averaged. To measure green fluorescence, the fluorometer was set at 485 nm for excitation and 529 nm for emission measurement. To measure red fluorescence, the fluorometer was set at 540 nm for excitation and 600 nm for emission measurement.

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