Further studies of the photoproduction of isolated photons with a jet at HERA

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ABSTRACT: In this extended analysis using the ZEUS detector at HERA, the photoproduction of isolated photons together with a jet is measured for different ranges of the fractional photon energy, $x_\gamma^{\text{meas}}$, contributing to the photon-jet final state. Cross sections are evaluated in the photon transverse-energy and pseudorapidity ranges $6 < E_\gamma^T < 15$ GeV and $-0.7 < \eta^\gamma < 0.9$, and for jet transverse-energy and pseudorapidity ranges $4 < E_\text{jet}^T < 35$ GeV and $-1.5 < \eta^\text{jet} < 1.8$, for an integrated luminosity of 374 pb$^{-1}$. The kinematic observables studied comprise the transverse energy and pseudorapidity of the photon and the jet, the azimuthal difference between them, the fraction of proton energy taking part in the interaction, and the difference between the pseudorapidities of the photon and the jet. Higher-order theoretical calculations are compared to the results.

KEYWORDS: Lepton-Nucleon Scattering, QCD, Photon production

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1 Introduction

In a recently published paper [1], the ZEUS collaboration presented cross sections for events containing an isolated high-energy photon, with and without a jet, produced in photoproduction at the HERA collider using the full HERA II data set. Such events can provide a direct probe of the underlying partonic process in high-energy collisions involving photons, since the emission of a high-energy photon is largely unaffected by parton hadronisation. In photoproduction processes in ep collisions at HERA, the exchanged virtual photon is quasi-real, with small virtuality, $Q^2$, conventionally required to be less than 1 GeV$^2$. These measurements follow earlier analyses of isolated photons in photoproduction by the ZEUS and H1 collaborations [2–7], as well as in deep inelastic scattering (DIS) [8–11]. In the analysis presented here, the most recent ZEUS photoproduction measurements are extended, using the same data as used previously.

In “direct” production processes, the entire incoming photon is absorbed by an outgoing quark from the incoming proton, while in “resolved” processes, the photon’s hadronic structure provides a quark or gluon that interacts with a parton from the proton. Figure 1 gives examples of the lowest-order (LO) direct and resolved diagrams for high-energy photoproduction of photons in quantum chromodynamics (QCD).  

Photons that are radiated in the hard scattering process, rather than resulting from meson decay, are commonly called “prompt”. An alternative nomenclature is to refer to such photons as “direct”; thus figures 1(a) and 1(b) would be called “direct-direct” and “resolved-direct” diagrams, respectively.
Figure 1. Examples of (a) direct-prompt and (b) resolved-prompt processes at leading order in QCD, and the related (c) direct and (d) resolved fragmentation processes.

also include “fragmentation processes” in which a photon is radiated within a jet, also illustrated in figure 1. Such processes are suppressed by requiring that the outgoing photon must be isolated.

Resolved and direct processes may be partially distinguished in events containing a high-$E_T$ photon and a jet by means of the quantity

$$x_{\text{meas}} = \frac{E_\gamma + E_{\text{jet}} - p_Z^\gamma - p_Z^{\text{jet}}}{E_{\text{all}} - p_Z^{\text{all}}},$$

which measures the fraction of the incoming photon energy that is given to the photon and the jet. The quantities $E_\gamma$ and $E_{\text{jet}}$ denote the energies of the photon and the jet, respectively, $p_Z$ denotes the corresponding longitudinal momenta, and the suffix “all”

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2The ZEUS coordinate system is a right-handed Cartesian system, with the Z axis pointing in the nominal proton beam direction, referred to as the “forward direction”, and the X axis pointing towards the centre of HERA. The coordinate origin is at the centre of the central tracking detector. The pseudorapidity is defined as $\eta = -\ln (\tan \frac{\theta}{2})$, where the polar angle, $\theta$, is measured with respect to the Z axis.
refers to all the measured final-state particles of an event. At LO, \( x_\gamma^{\text{meas}} = 1 \) for direct events, while any value in the range \((0,1)\) may be taken for resolved events. At higher order, the first statement no longer precisely holds, but the presence of direct processes generates a prominent peak in the cross section at high \( x_\gamma^{\text{meas}} \). Here, measurements in a direct-dominated region are presented by selecting events with \( x_\gamma^{\text{meas}} > 0.8 \), and in a resolved-dominated region by selecting events with \( x_\gamma^{\text{meas}} < 0.8 \). This enables the behaviour of the photoproduction process to be explored in more detail.

Several kinematic quantities are also measured beyond those presented previously. The quantity
\[
x_p^{\text{obs}} = \frac{(E_T^\gamma \exp(\eta^\gamma) + E_T^{\text{jet}} \exp(\eta^{\text{jet}}))}{2E_p}
\]
estimates the fraction of proton energy taken by the parton that interacts with the photon; its distribution is sensitive to the proton’s partonic structure. Here, \( E_T \) denotes transverse energy, \( \eta \) denotes pseudorapidity, and \( E_p \) is the energy of the proton beam. The difference in pseudorapidities, \( \eta^\gamma - \eta^{\text{jet}} \), is sensitive to the dynamical details of the hard scattering process, in particular to the spin of the exchanged quantum \([12]\). The quantity \( \Delta \phi \), defined as the absolute difference between the azimuths of the photon and the high-\( E_T \) jet, is sensitive to the presence of higher-order gluon radiation in the event, especially relative to the outgoing quark, which can generate non-collinearity between the photon and the leading jet. All three of these quantities are insensitive to Lorentz boosts along the \( Z \) axis.

Predictions from QCD-based models are compared to the measurements. The cross sections for isolated-photon production in photoproduction have been calculated to next-to-leading order (NLO) by Fontannaz, Guillet and Heinrich (FGH) \([13–15]\). Calculations based on the \( k_T \)-factorisation approach have been made by Lipatov, Malyshev and Zotov (LMZ) \([16–19]\).

2 Experimental set-up

The measurements are based on a data sample corresponding to an integrated luminosity of \( 374 \pm 7 \text{ pb}^{-1} \), taken during the years 2004 to 2007 with the ZEUS detector at HERA. During this period, HERA ran with an electron or positron beam energy of 27.5 GeV and a proton beam energy of \( E_p = 920 \text{ GeV} \). The sample is a sum of \( e^+ p \) and \( e^- p \) data.\(^3\)

A detailed description of the ZEUS detector can be found elsewhere \([20]\). Charged particles were measured in the central tracking detector (CTD) \([21–23]\) and a silicon micro vertex detector (MVD) \([24]\) which operated in a magnetic field of 1.43 T provided by a thin superconducting solenoid. The high-resolution uranium-scintillator calorimeter (CAL) \([25–28]\) consisted of three parts: the forward (FCAL), the barrel (BCAL) and the rear (RCAL) calorimeters. The BCAL covered the pseudorapidity range \(-0.74 \) to 1.01 as seen from the nominal interaction point, and the FCAL and RCAL extended the coverage to the range \(-3.5 \) to 4.0. Each part of the CAL was subdivided into elements referred to as cells. The barrel electromagnetic calorimeter (BEMC) cells had a pointing geometry aimed

\(^3\)Hereafter “electron” refers to both electrons and positrons unless otherwise stated.
at the nominal interaction point, with a cross section approximately $5 \times 20\,\text{cm}^2$, with the finer granularity in the $Z$ direction and the coarser in the $(X,Y)$ plane. This fine granularity allows the use of shower-shape distributions to distinguish isolated photons from the products of neutral meson decays such as $\pi^0 \to \gamma\gamma$. The CAL energy resolution, as measured under test-beam conditions, was $\sigma(E)/E = 0.18/\sqrt{E}$ for electrons and $0.35/\sqrt{E}$ for hadrons, where $E$ is in GeV.

The luminosity was measured [29] using the Bethe-Heitler reaction $ep \to e\gamma p$ by a luminosity detector which consisted of two independent systems: a lead-scintillator calorimeter [30–32] and a magnetic spectrometer [33].

3 Theoretical models

Two theoretical models are considered. In the approach of FGH [13, 14], the LO and NLO diagrams and the box-diagram term are calculated explicitly. Fragmentation processes are calculated in terms of a fragmentation function in which a quark or gluon gives rise to a photon; an experimentally determined non-perturbative parameterisation is used as input to the theoretical calculation [34]. Fragmentation and box terms each contribute about 10% to the total cross section. The CTEQ6 [35] and AFG04 [36] parton densities are used for the proton and photon, respectively. Theoretical uncertainties arise due to the choice of renormalisation, factorisation and fragmentation scales. They were estimated, using a more conservative approach [15] than in the original published paper [13], by varying the renormalisation scale by factors of 0.5 and 2.0, since this gave the largest effect on the cross sections.

The $k_T$-factorisation method used by LMZ [16–18] makes use of unintegrated parton densities in the proton, using the KMR formalism [37, 38] based on the MSTW08 proton parton densities [39]. In addition to the hard QCD subprocess, the model incorporates a parton evolution cascade, one jet from which can be taken as the leading jet in the analysis. Fragmentation terms and the quark content of the resolved photon are not included, but the box diagram is included together with $2 \to 3$ subprocesses to represent the LO direct and resolved photon contributions. The calculation used in the previous ZEUS analysis [1] has been augmented by a term that takes account of the gluon content of the resolved photon, and further technical changes have been implemented [19]. Uncertainties associated with the hard scale were provided by the authors. There is a further overall statistical uncertainty on the set of results for each variable, of the order of 10% for the results presented here.

All results are presented at the hadron level; to make use of the theoretical predictions, cuts equivalent to the experimental kinematic selections including the photon isolation (see section 5) were applied at the parton level. Hadronisation corrections were then evaluated (section 4) and applied to the theoretical calculations to enable a comparison to the experimental data.
4 Monte Carlo event simulation

Monte Carlo (MC) event samples were employed to evaluate the detector acceptance and event-reconstruction efficiency, and to provide signal and background distributions. The program PYTHIA 6.416 [40] was used to generate the direct and resolved prompt-photon processes at LO, and also $2 \to 2$ parton-parton scattering processes not involving photons ("dijet events"), making use of the CTEQ4 [41] and GRV [42, 43] proton and photon parton densities. The program was run using the default parameters with minor modifications. The isolated photons measured in the experiment are accompanied by backgrounds from neutral mesons in hadronic jets, in particular $\pi^0$ and $\eta$, where the meson decay products create an energy cluster in the BCAL that passes the selection criteria for a photon. The dijet event samples included background events of this kind which were extracted for use in the analysis. The PYTHIA dijet events in which a high-energy photon was radiated from a quark or lepton ("radiative events") were not used in the background samples but were defined, in accordance with theory, as a component of the signal.

Event samples were also generated using the HERWIG 6.510 program [44], again with minor modifications to the default parameters. The PYTHIA and HERWIG programs differ significantly in their treatment of parton showers, and in the use of a string-based hadronisation scheme in PYTHIA but a cluster-based scheme in HERWIG.

The generated MC events were passed through the ZEUS detector and trigger simulation programs based on GEANT 3.21 [45]. They were then reconstructed and analysed using the same programs as used for the data. The hadronisation corrections to the theory calculations were evaluated using PYTHIA and HERWIG, the two programs being in agreement to a few percent; PYTHIA was used to provide the values for the present analysis. No uncertainties were applied to these corrections. They were calculated by running the same jet algorithm and event selections, including the isolation criterion, on the generated partons and on the hadronised final state in the direct and resolved prompt-photon MC events.

5 Event selection and reconstruction

The basic event selection and reconstruction was performed as previously. A three-level trigger system was used to select events online [20, 46, 47]:

- the first-level trigger required a loosely measured track in the CTD and a minimum energy deposited in the CAL;
- at the second level, the event conditions were tightened;
- at the third level, the event was reconstructed and a high-energy photon candidate was required. Most deep inelastic scattering events were rejected.

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4In particular, the PYTHIA parameter $\text{PARP}(67)$ was set to 4.0 and multiple parton interactions were turned off. In HERWIG the parameters $\text{ISPAC}$, $\text{QSPAC}$, and $\text{PTRMS}$ were set to 2, 4.0, and 0.44.
In the offline event analysis, some general conditions were applied as follows:

- to reduce background from non-ep collisions, events were required to have a reconstructed vertex position, \( Z_{vtx} \), within the range \( |Z_{vtx}| < 40 \text{ cm} \);
- to remove any DIS contamination, no scattered beam electron was permitted in the ZEUS detector;
- a range of incoming virtual photon energies was selected by the requirement \( 0.2 < y_{JB} < 0.7 \), where \( y_{JB} = \sum_i E_i (1 - \cos \theta_i)/2E_e \) and \( E_e \) is the energy of the electron beam. Here, \( E_i \) is the energy of the \( i \)-th CAL cell, \( \theta_i \) is its polar angle and the sum runs over all cells [48]. The lower cut strengthened the trigger requirements and the upper cut further suppressed remaining deep inelastic scattering events.

The subsequent event analysis made use of energy-flow objects (EFOs) [49, 50], which were constructed from clusters of calorimeter cells, associated with tracks when appropriate. Tracks not associated with calorimeter clusters were also used. Photon candidates were EFOs with no associated track and with at least 90% of the reconstructed energy measured in the BEMC. Candidate EFOs with wider electromagnetic showers than are typical for a single photon were accepted, in order to evaluate the backgrounds.

Jet reconstruction was performed, making use of all the EFOs in the event including photon candidates, by means of the \( k_T \) clustering algorithm [51] in the \( E \)-scheme in the longitudinally invariant inclusive mode [52] with the radius parameter set to 1.0. By construction, one of the jets found by this procedure corresponds to or includes the photon candidate. An additional accompanying jet was required; if more than one was found in the designated angular range, that with the highest transverse energy, \( E_{\text{jet}}^T \), was used. In the kinematic region used, the resolution of the jet transverse energy was about 15–20%, estimated using MC simulations.

To reduce the fragmentation contribution and the background from the decay of neutral mesons within jets, the photon candidate was required to be isolated from other hadronic activity. This was imposed by requiring that the photon-candidate EFO had at least 90% of the total energy of the reconstructed jet of which it formed a part. High-\( E_T \) photons radiated from scattered leptons were further suppressed by rejecting photons with a nearby track. This was achieved by demanding \( \Delta R > 0.2 \), where \( \Delta R = \sqrt{\Delta \phi^2 + (\Delta \eta)^2} \) is the distance to the nearest reconstructed track with momentum greater than 250 MeV in the \( \eta - \phi \) plane, where \( \phi \) is the azimuthal angle. This latter condition was applied only at the detector level, and not in the hadron- or parton-level calculations.

Events were finally selected with the following kinematic conditions:

- each event was required to contain an isolated photon candidate with a reconstructed transverse energy, \( E_T^\gamma \), in the range \( 6 < E_T^\gamma < 15 \text{ GeV} \) and with pseudorapidity, \( \eta^\gamma \), in the range \( -0.7 < \eta^\gamma < 0.9 \);
- a hadronic jet was required with \( E_{\text{jet}}^T \) between 4 and 35 GeV and lying within the pseudorapidity, \( \eta^{\text{jet}} \), range \( -1.5 < \eta^{\text{jet}} < 1.8 \);
• selections were made for all \( x_\gamma^{\text{meas}} \), giving a total of 12450 events, and for \( x_\gamma^{\text{meas}} > 0.8 \) and \( x_\gamma^{\text{meas}} < 0.8 \). The latter two conditions selected events in direct-enhanced and resolved-enhanced regions, respectively. An additional selection was made with events having \( x_\gamma^{\text{meas}} < 0.7 \).

6 Extraction of the photon signal

The selected samples contain a large admixture of background events in which one or more neutral mesons, such as \( \pi^0 \) and \( \eta \), have decayed to photons, thereby producing a photon candidate in the BEMC. The photon signal was extracted statistically following the approach used in previous ZEUS analyses [1, 8–11]. The method made use of the energy-weighted width, measured in the \( Z \) direction, of the BEMC energy-cluster comprising the photon candidate. This width was calculated as

\[
\langle \delta Z \rangle = \frac{\sum_i E_i |Z_i - Z_{\text{cluster}}|}{w_{\text{cell}} \sum_i E_i},
\]

where \( Z_i \) is the \( Z \) position of the centre of the \( i \)-th cell, \( Z_{\text{cluster}} \) is the energy-weighted centroid of the EFO cluster, \( w_{\text{cell}} \) is the width of the cell in the \( Z \) direction, and \( E_i \) is the energy recorded in the cell. The sum runs over all BEMC cells in the EFO.

The number of isolated-photon events in the data was determined by a \( \chi^2 \) fit to the \( \langle \delta Z \rangle \) distribution in the range 0.05 < \( \langle \delta Z \rangle \) < 0.8, varying the relative fractions of the signal and background components as represented by histogram templates obtained from the MC. The fit was performed for each measured cross-section bin, with \( \chi^2 \) values of typically 1.1 per degree of freedom (e.g. 31/28), verifying that the signal and background were well understood. The extracted signals corresponded overall to 6262\( \pm \)132 events with a photon and an accompanying jet. A set of typical fits for different ranges of the photon transverse energy is shown in figure 2 and illustrates how the signal-to-background ratio improves with increasing \( E_\gamma^T \).

A bin-by-bin correction method was used to determine the production cross section in a given variable, by means of the relationship

\[
\frac{d\sigma}{dY} = \frac{A N(\gamma)}{L \Delta Y},
\]

where \( N(\gamma) \) is the number of photons in a bin as extracted from the fit, \( \Delta Y \) is the bin width, \( L \) is the total integrated luminosity, and \( A \) is the acceptance correction. The acceptance correction was calculated, using MC samples, as the ratio of the number of events that were generated in the given bin to the number of events obtained in the bin after event reconstruction. Its value was typically 1.2.

Allowance must be made for the different acceptances for the direct and the resolved processes, as modelled by PYTHIA. Over the entire \( x_\gamma^{\text{meas}} \) range, a reasonable phenomenological description of the data can be obtained using a MC sample consisting of a 50:40 mixture of PYTHIA-simulated direct and resolved events, normalised to the data, with a 10% admixture of radiative events divided equally between direct and resolved. The acceptance factors were calculated using this model, applying selections for the chosen \( x_\gamma^{\text{meas}} \)
Figure 2. Examples of fits to $\langle \delta Z \rangle$ for different ranges of the photon transverse energy, showing the signal and background contributions and the fitted total.

regions. Small corrections were applied for the trigger efficiency modelling and a residual contamination by DIS events [1].

The photon energy scale was calibrated by means of an analysis of deeply virtual Compton scattering events recorded by ZEUS, in which the detected final-state particles comprised a scattered electron, whose energy measurement is well understood, and a balancing outgoing photon.

7 Systematic uncertainties

The most significant sources of systematic uncertainty were evaluated as follows:

- to allow for uncertainties in the simulation of the hadronic final state, the cross sections were recalculated using HERWIG to model the signal and background events. The ensuing changes in the results correspond to an uncertainty of typically up to 8%, but rising to 18% in the highest bin of $x_\gamma^{\text{meas}}$;

- the energy of the photon candidate was varied by $\pm 2\%$ in the MC at the detector level. Independently, the energy of the accompanying jet was varied by an amount decreasing from $\pm 4.5\%$ to $\pm 2.5\%$ as $E_T^{\text{jet}}$ increases from 4 GeV to above 10 GeV. Each of these gave variations in the measured cross sections of typically 5%.
Further systematic uncertainties were evaluated as follows:

- the uncertainty in the acceptance due to the estimation of the relative fractions of direct and resolved events and radiative events in the MC sample was estimated by varying these fractions by $\pm 15\%$ and $\pm 5\%$ respectively in absolute terms; the changes in the cross sections were typically $\pm 2\%$ in each case;

- the dependence of the result on the modelling of the hadronic background by the MC was investigated by varying the upper limit for the $\langle \delta Z \rangle$ fit in the range $[0.6, 1.0]$; this gave a $\pm 2\%$ variation;

- the $E_T^\gamma$, $\eta^{\text{jet}}$ and $\Delta\phi$ distributions in the MC were reweighted simultaneously to provide a closer agreement with the data, and the cross sections were re-evaluated. This generated changes of typically $\pm 2\%$.

Other sources of systematic uncertainty were found to be negligible. These included the modelling of the track-isolation cut and the track-momentum cut, and also the cuts on photon isolation, the electromagnetic fraction of the photon shower, $y_{\text{JB}}$ and $Z_{\text{vtx}}$. Except for the uncertainty on the modelling of the hadronic final state, the major uncertainties were treated as symmetric, and all the uncertainties were combined in quadrature. The uncertainties of 2.0% on the trigger efficiency and 1.9% on the luminosity measurement were not included in the tables and figures.

8 Results

Differential cross sections were calculated for the production of an isolated photon with at least one accompanying jet, in the kinematic region defined by $Q^2 < 1\text{ GeV}^2$, $0.2 < y < 0.7$, $-0.7 < \eta^\gamma < 0.9$, $6 < E_T^\gamma < 15\text{ GeV}$, $4 < E_T^{\text{jet}} < 35\text{ GeV}$ and $-1.5 < \eta^{\text{jet}} < 1.8$. All quantities were evaluated at the hadron level in the laboratory frame, and $y$ is defined as the fraction of the incoming lepton energy that is given to the virtual photon. The jets were formed according to the $k_T$ clustering algorithm with the radius parameter set to 1.0. Photon isolation was imposed such that at least 90% of the energy of the jet-like object containing the photon originated from the photon. If more than one accompanying jet was found within the designated $\eta^{\text{jet}}$ range in an event, that with highest $E_T^{\text{jet}}$ was taken. Cross sections in $E_T^{\text{jet}}$ above 15 GeV are omitted from the tables and figure 4 owing to limited statistics, but this kinematic region is included in the other cross-section measurements.

Complementing the previously published cross sections [1] for the entire $x_{\gamma}\text{meas}$ range, differential cross sections as functions of $E_T^\gamma$, $\eta^\gamma$, $E_T^{\text{jet}}$ and $\eta^{\text{jet}}$ are shown in figures 3–4. Here the selections of $x_{\gamma}\text{meas} > 0.8$ and $x_{\gamma}\text{meas} < 0.8$ have been applied to define ranges that enhance the direct and resolved processes. In the PYTHIA model that was used, the upper and lower $x_{\gamma}\text{meas}$ ranges contain direct and resolved events in the ratios 86:14 and 22:78, respectively.

To within the theoretical uncertainties, the cross section predicted by FGH is in quantitative agreement with the data; the LMZ predicted cross section also agrees well for the photon and $E_T^{\text{jet}}$ variables, but it is in disagreement with the $\eta^{\text{jet}}$ distribution for
\( x^{\text{meas}} < 0.8 \). This disagreement may be due to the modelling of the jet from the parton cascade in the present version of the LMZ model.

The variables \( x^{\text{obs}}_p \) and \( \eta^{\gamma} - \eta^{\text{jet}} \), presented in figures 5 and 6, also include results evaluated for the entire \( x^{\gamma \text{meas}} \) range. They are well described by FGH but slightly less so by LMZ.

Differential cross sections as functions of \( \Delta \phi \) are shown in figure 7. The data are compared to FGH and LMZ, with similar conclusions as before, and are also compared to the versions of PYTHIA and HERWIG described in section 4. The MC programs both give a reasonable description of the data. These results demonstrate that parton showers used in conjunction with LO MC programs can give a good description of higher-order contributions, as also observed in other reactions [53–55].

Tables 1 to 6 give the numerical values of the above results, together with the hadronisation factors that were applied to the theory. For further information, cross sections calculated in the range \( x^{\gamma \text{meas}} < 0.7 \) are also listed. These have a direct:resolved ratio of 15:85 as modelled by PYTHIA and show features that are similar to the plotted results.
9 Conclusions

The production of isolated photons with an accompanying jet has been measured in photoproduction with the ZEUS detector at HERA using an integrated luminosity of 374 ± 7 pb$^{-1}$. The present measurements extend earlier ZEUS results. Differential cross sections are presented in a kinematic region defined in the laboratory frame by: $Q^2 < 1$ GeV$^2$, $0.2 < y < 0.7$, $-0.7 < \eta^{\gamma} < 0.9$, $6 < E_T^{\gamma} < 15$ GeV, $4 < E_T^{\text{jet}} < 35$ GeV and $-1.5 < \eta^{\text{jet}} < 1.8$. Photon isolation was imposed such that at least 90% of the energy of the jet-like object containing the photon originated from the photon.

Differential cross sections are given in terms of the transverse energy and pseudorapidity of the photon and the jet, and in terms of $x_{\gamma}^{\text{obs}}$, $\eta^{\gamma} - \eta^{\text{jet}}$ and $\Delta \phi$ in high and low regions of $x_{\gamma}^{\text{meas}}$. The latter three variables are also presented for the entire observed $x_{\gamma}^{\text{meas}}$ range. The NLO-based predictions of Fontannaz, Guillet and Heinrich reproduce all the measured experimental distributions well. The $k_T$-factorisation approach of Lipatov, Malyshev and Zotov describes most of the distributions well, with the exception of the jet pseudorapidity at low $x_{\gamma}^{\text{meas}}$. 

Figure 4. Differential cross sections as functions of (a, c) $E_T^{\text{jet}}$ and (b, d) $\eta^{\text{jet}}$, for events containing an isolated photon accompanied by a jet, compared to predictions from FGH and LMZ. The first two FGH points in (a, c) have been averaged into a single bin for calculational reasons. Other details as for figure 3.
Figure 5. Differential cross sections as functions of $x_p^{\text{obs}}$ for (a) all $x_\gamma^{\text{meas}}$, (b) $x_\gamma^{\text{meas}} > 0.8$ (c) $x_\gamma^{\text{meas}} < 0.8$ for events containing an isolated photon accompanied by a jet, compared to predictions from FGH and LMZ. Other details as for figure 3.
Figure 6. Differential cross sections as functions of $\eta^{\gamma} - \eta^{\text{jet}}$ for (a) all $x_{\gamma}^{\text{meas}}$, (b) $x_{\gamma}^{\text{meas}} > 0.8$ (c) $x_{\gamma}^{\text{meas}} < 0.8$ for events containing an isolated photon accompanied by a jet, compared to predictions from FGH and LMZ. Other details as for figure 3.
Figure 7. Differential cross sections as functions of $\Delta \phi$ for (a) all $x_{\gamma}^{\text{meas}}$, (b) $x_{\gamma}^{\text{meas}} > 0.8$ (c) $x_{\gamma}^{\text{meas}} < 0.8$ for events containing an isolated photon accompanied by a jet, compared to predictions from FGH, LMZ, PYTHIA and HERWIG. Other details as for figure 3.
$$E_T^\gamma$$ range
\begin{tabular}{|c|c|c|}
\hline
\(x_\gamma^\text{meas} \geq 0.8\) & \(\frac{d\sigma}{dE_T^\gamma}\) (pb GeV\(^{-1}\)) & had. corr. \\
\hline
6.0 – 7.0 & 3.79 ± 0.26 (stat.) +0.37 \(^{+0.27}_{-0.16}\) (syst.) & 0.84 \\
7.0 – 8.5 & 2.60 ± 0.17 (stat.) +0.23 \(^{+0.23}_{-0.14}\) (syst.) & 0.90 \\
8.5 – 10.0 & 1.55 ± 0.13 (stat.) +0.21 \(^{+0.21}_{-0.13}\) (syst.) & 0.96 \\
10.0 – 15.0 & 0.63 ± 0.04 (stat.) +0.04 \(^{+0.04}_{-0.04}\) (syst.) & 0.98 \\
\hline
\(x_\gamma^\text{meas} < 0.8\) & & \\
\hline
6.0 – 7.0 & 3.22 ± 0.24 (stat.) +0.34 \(^{+0.25}_{-0.26}\) (syst.) & 0.79 \\
7.0 – 8.5 & 2.07 ± 0.14 (stat.) +0.15 \(^{+0.15}_{-0.09}\) (syst.) & 0.80 \\
8.5 – 10.0 & 1.06 ± 0.10 (stat.) +0.07 \(^{+0.09}_{-0.07}\) (syst.) & 0.81 \\
10.0 – 15.0 & 0.27 ± 0.03 (stat.) +0.02 \(^{+0.03}_{-0.03}\) (syst.) & 0.83 \\
\hline
\(x_\gamma^\text{meas} < 0.7\) & & \\
\hline
6.0 – 7.0 & 2.37 ± 0.21 (stat.) +0.29 \(^{+0.26}_{-0.21}\) (syst.) & 0.72 \\
7.0 – 8.5 & 1.32 ± 0.12 (stat.) +0.10 \(^{+0.09}_{-0.09}\) (syst.) & 0.75 \\
8.5 – 10.0 & 0.66 ± 0.09 (stat.) +0.07 \(^{+0.07}_{-0.07}\) (syst.) & 0.77 \\
10.0 – 15.0 & 0.18 ± 0.03 (stat.) +0.02 \(^{+0.02}_{-0.02}\) (syst.) & 0.80 \\
\hline
\end{tabular}

Table 1. Differential cross-section \(\frac{d\sigma}{dE_T^\gamma}\) for photons accompanied by a jet, and hadronisation correction.

\(\eta^\gamma\) range
\begin{tabular}{|c|c|c|}
\hline
\(x_\gamma^\text{meas} > 0.8\) & \(\frac{d\sigma}{d\eta^\gamma}\) (pb) & had. corr. \\
\hline
-0.7 – -0.3 & 10.69 ± 0.62 (stat.) +1.20 \(^{+1.20}_{-0.71}\) (syst.) & 0.93 \\
-0.3 – 0.1 & 10.07 ± 0.59 (stat.) +0.66 \(^{+0.66}_{-0.63}\) (syst.) & 0.93 \\
0.1 – 0.5 & 7.06 ± 0.56 (stat.) +0.51 \(^{+0.51}_{-0.36}\) (syst.) & 0.90 \\
0.5 – 0.9 & 4.00 ± 0.50 (stat.) +0.36 \(^{+0.36}_{-0.20}\) (syst.) & 0.87 \\
\hline
\(x_\gamma^\text{meas} < 0.8\) & & \\
\hline
-0.7 – -0.3 & 4.54 ± 0.40 (stat.) +0.41 \(^{+0.41}_{-0.42}\) (syst.) & 0.84 \\
-0.3 – 0.1 & 6.83 ± 0.44 (stat.) +0.46 \(^{+0.47}_{-0.46}\) (syst.) & 0.80 \\
0.1 – 0.5 & 7.20 ± 0.48 (stat.) +0.37 \(^{+0.37}_{-0.38}\) (syst.) & 0.80 \\
0.5 – 0.9 & 4.08 ± 0.51 (stat.) +0.43 \(^{+0.43}_{-0.21}\) (syst.) & 0.79 \\
\hline
\(x_\gamma^\text{meas} < 0.7\) & & \\
\hline
-0.7 – -0.3 & 2.79 ± 0.31 (stat.) +0.26 \(^{+0.26}_{-0.27}\) (syst.) & 0.78 \\
-0.3 – 0.1 & 4.56 ± 0.38 (stat.) +0.31 \(^{+0.31}_{-0.31}\) (syst.) & 0.74 \\
0.1 – 0.5 & 5.12 ± 0.44 (stat.) +0.32 \(^{+0.32}_{-0.32}\) (syst.) & 0.74 \\
0.5 – 0.9 & 3.15 ± 0.49 (stat.) +0.43 \(^{+0.43}_{-0.26}\) (syst.) & 0.74 \\
\hline
\end{tabular}

Table 2. Differential cross-section \(\frac{d\sigma}{d\eta^\gamma}\) for photons accompanied by a jet, and hadronisation correction.
Table 3. Differential cross-section $\frac{d\sigma}{dE_T^{\gamma}}$ for photons accompanied by a jet, and hadronisation correction.

| $E_T^{\gamma \text{jet}}$ range (GeV) | $\frac{d\sigma}{dE_T^{\gamma}}$ (pb GeV$^{-1}$) | had. corr. |
|--------------------------------------|------------------------------------------|-----------|
| $x_T^{\gamma \text{meas}} > 0.8$    | 4.0  -  6.0  1.29 ± 0.10 (stat.) $^{+0.21}_{-0.16}$ (syst.) | 0.81     |
|                                      | 6.0  -  8.0  2.13 ± 0.14 (stat.) $^{+0.23}_{-0.15}$ (syst.) | 0.83     |
|                                      | 8.0  - 10.0  1.56 ± 0.12 (stat.) $^{+0.12}_{-0.14}$ (syst.) | 0.96     |
|                                      | 10.0 - 15.0  0.59 ± 0.04 (stat.) $^{+0.07}_{-0.05}$ (syst.) | 1.05     |
| $x_T^{\gamma \text{meas}} < 0.8$    | 4.0  -  6.0  1.43 ± 0.10 (stat.) $^{+0.17}_{-0.16}$ (syst.) | 0.84     |
|                                      | 6.0  -  8.0  1.29 ± 0.10 (stat.) $^{+0.09}_{-0.08}$ (syst.) | 0.73     |
|                                      | 8.0  - 10.0  1.06 ± 0.09 (stat.) $^{+0.10}_{-0.17}$ (syst.) | 0.80     |
|                                      | 10.0 - 15.0  0.28 ± 0.03 (stat.) $^{+0.02}_{-0.04}$ (syst.) | 0.87     |
| $x_T^{\gamma \text{meas}} < 0.7$    | 4.0  -  6.0  1.07 ± 0.09 (stat.) $^{+0.15}_{-0.08}$ (syst.) | 0.76     |
|                                      | 6.0  -  8.0  0.82 ± 0.09 (stat.) $^{+0.05}_{-0.05}$ (syst.) | 0.68     |
|                                      | 8.0  - 10.0  0.73 ± 0.08 (stat.) $^{+0.07}_{-0.14}$ (syst.) | 0.77     |
|                                      | 10.0 - 15.0  0.20 ± 0.03 (stat.) $^{+0.02}_{-0.03}$ (syst.) | 0.83     |

Table 4. Differential cross-section $\frac{d\sigma}{dp_T^{\gamma}}$ for photons accompanied by a jet, and hadronisation correction.
\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|}
\hline
\multicolumn{2}{|c|}{\(x_{\gamma}^{\text{obs}}\) range} & \multicolumn{1}{|c|}{\(\frac{d\sigma}{dx_{\gamma}^{\text{meas}}}\) (pb)} & had. corr. \\
\hline
All \(x_{\gamma}^{\text{meas}}\) & & & \\
0.0 – 0.005 & 297.6 ± 30.4 (stat.) \(+\frac{46.0}{-51.3}\) (syst.) & 0.76 & \\
0.005 – 0.010 & 1471.5 ± 63.2 (stat.) \(+\frac{135.3}{-124.3}\) (syst.) & 0.80 & \\
0.010 – 0.015 & 1160.0 ± 57.5 (stat.) \(+\frac{56.9}{-57.2}\) (syst.) & 0.90 & \\
0.015 – 0.025 & 514.5 ± 27.8 (stat.) \(+\frac{20.5}{-21.4}\) (syst.) & 0.94 & \\
0.025 – 0.040 & 130.1 ± 11.7 (stat.) \(+\frac{46.0}{-51.3}\) (syst.) & 0.99 & \\
0.040 – 0.070 & 12.6 ± 2.6 (stat.) \(+\frac{10.0}{-3.8}\) (syst.) & 1.00 & \\
\hline
\multicolumn{2}{|c|}{\(x_{\gamma}^{\text{meas}} > 0.8\)} & & \\
0.0 – 0.005 & 199.5 ± 27.3 (stat.) \(+\frac{23.2}{-28.8}\) (syst.) & 0.72 & \\
0.005 – 0.010 & 975.3 ± 54.4 (stat.) \(+\frac{81.8}{-68.1}\) (syst.) & 0.82 & \\
0.010 – 0.015 & 662.8 ± 46.7 (stat.) \(+\frac{68.4}{-28.8}\) (syst.) & 1.00 & \\
0.015 – 0.025 & 276.9 ± 21.3 (stat.) \(+\frac{21.4}{-15.3}\) (syst.) & 1.12 & \\
0.025 – 0.040 & 61.9 ± 8.0 (stat.) \(+\frac{4.3}{-4.3}\) (syst.) & 1.26 & \\
0.040 – 0.070 & 0.9 ± 0.9 (stat.) \(+\frac{1.5}{-0.6}\) (syst.) & 1.29 & \\
\hline
\multicolumn{2}{|c|}{\(x_{\gamma}^{\text{meas}} < 0.8\)} & & \\
0.0 – 0.005 & 79.6 ± 14.8 (stat.) \(+\frac{20.7}{-31.4}\) (syst.) & 0.95 & \\
0.005 – 0.010 & 492.3 ± 37.0 (stat.) \(+\frac{52.3}{-53.5}\) (syst.) & 0.77 & \\
0.010 – 0.015 & 515.2 ± 38.1 (stat.) \(+\frac{24.7}{-28.0}\) (syst.) & 0.78 & \\
0.015 – 0.025 & 249.9 ± 20.6 (stat.) \(+\frac{14.0}{-21.9}\) (syst.) & 0.81 & \\
0.025 – 0.040 & 70.9 ± 9.4 (stat.) \(+\frac{4.7}{-6.1}\) (syst.) & 0.85 & \\
0.040 – 0.070 & 5.3 ± 2.2 (stat.) \(+\frac{0.9}{-1.0}\) (syst.) & 0.86 & \\
\hline
\multicolumn{2}{|c|}{\(x_{\gamma}^{\text{meas}} < 0.7\)} & & \\
0.0 – 0.005 & 35.5 ± 11.4 (stat.) \(+\frac{9.4}{-10.4}\) (syst.) & 0.69 & \\
0.005 – 0.010 & 298.3 ± 30.4 (stat.) \(+\frac{34.9}{-39.5}\) (syst.) & 0.68 & \\
0.010 – 0.015 & 366.1 ± 33.5 (stat.) \(+\frac{21.0}{-21.6}\) (syst.) & 0.73 & \\
0.015 – 0.025 & 193.6 ± 18.8 (stat.) \(+\frac{12.6}{-21.6}\) (syst.) & 0.78 & \\
0.025 – 0.040 & 51.4 ± 9.0 (stat.) \(+\frac{2.1}{-4.8}\) (syst.) & 0.83 & \\
0.040 – 0.070 & 3.8 ± 2.1 (stat.) \(+\frac{1.1}{-0.9}\) (syst.) & 0.82 & \\
\hline
\end{tabular}
\caption{Differential cross-section \(\frac{d\sigma}{dx_{\gamma}^{\text{meas}}}\) for photons accompanied by a jet, and hadronisation correction.}
\end{table}
\( (\eta^\gamma - \eta^{\text{jet}}) \) range & \( \frac{d\sigma}{d(\eta^\gamma - \eta^{\text{jet}})} \) (pb) & had. corr. \\
\hline
All \( x_{\gamma}^{\text{meas}} \) & & \\
\( -2.2 \) & \( -1.5 \) & \( 3.17 \pm 0.24 \) (stat.) \(+0.14\) (syst.) \( 1.04 \) \\
\( -1.5 \) & \( -0.8 \) & \( 6.56 \pm 0.35 \) (stat.) \(+0.31\) (syst.) \( 0.96 \) \\
\( -0.8 \) & \( -0.1 \) & \( 8.57 \pm 0.40 \) (stat.) \(+0.58\) (syst.) \( 0.89 \) \\
\( -0.1 \) & \( 0.6 \) & \( 7.42 \pm 0.38 \) (stat.) \(+0.52\) (syst.) \( 0.84 \) \\
\( 0.6 \) & \( 1.3 \) & \( 3.99 \pm 0.32 \) (stat.) \(+0.23\) (syst.) \( 0.77 \) \\
\( 1.3 \) & \( 2.0 \) & \( 0.98 \pm 0.19 \) (stat.) \(+0.14\) (syst.) \( 0.73 \) \\
\hline
\( x_{\gamma}^{\text{meas}} > 0.8 \) & & \\
\( -2.2 \) & \( -1.5 \) & \( 1.81 \pm 0.19 \) (stat.) \(+0.35\) (syst.) \( 1.32 \) \\
\( -1.5 \) & \( -0.8 \) & \( 3.41 \pm 0.26 \) (stat.) \(+0.33\) (syst.) \( 1.18 \) \\
\( -0.8 \) & \( -0.1 \) & \( 4.44 \pm 0.31 \) (stat.) \(+0.53\) (syst.) \( 1.04 \) \\
\( -0.1 \) & \( 0.6 \) & \( 4.88 \pm 0.34 \) (stat.) \(+0.37\) (syst.) \( 0.88 \) \\
\( 0.6 \) & \( 1.3 \) & \( 2.77 \pm 0.29 \) (stat.) \(+0.18\) (syst.) \( 0.74 \) \\
\( 1.3 \) & \( 2.0 \) & \( 0.74 \pm 0.18 \) (stat.) \(+0.09\) (syst.) \( 0.65 \) \\
\hline
\( x_{\gamma}^{\text{meas}} < 0.8 \) & & \\
\( -2.2 \) & \( -1.5 \) & \( 1.49 \pm 0.17 \) (stat.) \(+0.08\) (syst.) \( 0.89 \) \\
\( -1.5 \) & \( -0.8 \) & \( 3.34 \pm 0.27 \) (stat.) \(+0.23\) (syst.) \( 0.83 \) \\
\( -0.8 \) & \( -0.1 \) & \( 4.23 \pm 0.29 \) (stat.) \(+0.34\) (syst.) \( 0.75 \) \\
\( -0.1 \) & \( 0.6 \) & \( 2.63 \pm 0.24 \) (stat.) \(+0.24\) (syst.) \( 0.76 \) \\
\( 0.6 \) & \( 1.3 \) & \( 1.24 \pm 0.18 \) (stat.) \(+0.10\) (syst.) \( 0.88 \) \\
\( 1.3 \) & \( 2.0 \) & \( 0.19 \pm 0.09 \) (stat.) \(+0.07\) (syst.) \( 1.15 \) \\
\hline
\( x_{\gamma}^{\text{meas}} < 0.7 \) & & \\
\( -2.2 \) & \( -1.5 \) & \( 1.02 \pm 0.15 \) (stat.) \(+0.08\) (syst.) \( 0.85 \) \\
\( -1.5 \) & \( -0.8 \) & \( 2.56 \pm 0.25 \) (stat.) \(+0.18\) (syst.) \( 0.81 \) \\
\( -0.8 \) & \( -0.1 \) & \( 3.19 \pm 0.27 \) (stat.) \(+0.24\) (syst.) \( 0.72 \) \\
\( -0.1 \) & \( 0.6 \) & \( 1.69 \pm 0.21 \) (stat.) \(+0.24\) (syst.) \( 0.68 \) \\
\( 0.6 \) & \( 1.3 \) & \( 0.61 \pm 0.15 \) (stat.) \(+0.08\) (syst.) \( 0.71 \) \\
\( 1.3 \) & \( 2.0 \) & \( 0.00 \pm 0.48 \) (stat.) \(+0.13\) (syst.) \( 0.87 \) \\
\hline

Table 6. Differential cross-section \( \frac{d\sigma}{d(\eta^\gamma - \eta^{\text{jet}})} \) for photons accompanied by a jet, and hadronisation correction.
| $\Delta \phi$ range (deg.) | $\frac{d\sigma}{d\Delta \phi}$ (pb deg. $^{-1}$) | had. corr. |
|-------------------------|---------------------------------|--------|
| All $x_\gamma^{\text{meas}}$ | | |
| 0.0 – 90.0 | $0.0048 \pm 0.0010$ (stat.) $^{+0.0032}_{-0.0013}$ (syst.) | 0.78 |
| 90.0 – 130.0 | $0.033 \pm 0.004$ (stat.) $^{+0.005}_{-0.002}$ (syst.) | 0.81 |
| 130.0 – 140.0 | $0.100 \pm 0.012$ (stat.) $^{+0.013}_{-0.009}$ (syst.) | 0.82 |
| 140.0 – 150.0 | $0.164 \pm 0.016$ (stat.) $^{+0.018}_{-0.014}$ (syst.) | 0.85 |
| 150.0 – 160.0 | $0.296 \pm 0.019$ (stat.) $^{+0.027}_{-0.016}$ (syst.) | 0.86 |
| 160.0 – 170.0 | $0.473 \pm 0.026$ (stat.) $^{+0.019}_{-0.026}$ (syst.) | 0.89 |
| 170.0 – 180.0 | $0.951 \pm 0.036$ (stat.) $^{+0.030}_{-0.066}$ (syst.) | 0.86 |
| $x_\gamma^{\text{meas}} > 0.8$ | | |
| 0.0 – 90.0 | $0.002 \pm 0.001$ (stat.) $^{+0.0010}_{-0.0002}$ (syst.) | 0.57 |
| 90.0 – 130.0 | $0.012 \pm 0.003$ (stat.) $^{+0.001}_{-0.001}$ (syst.) | 0.76 |
| 130.0 – 140.0 | $0.026 \pm 0.008$ (stat.) $^{+0.005}_{-0.009}$ (syst.) | 0.77 |
| 140.0 – 150.0 | $0.051 \pm 0.010$ (stat.) $^{+0.015}_{-0.006}$ (syst.) | 0.85 |
| 150.0 – 160.0 | $0.140 \pm 0.014$ (stat.) $^{+0.037}_{-0.006}$ (syst.) | 0.89 |
| 160.0 – 170.0 | $0.295 \pm 0.022$ (stat.) $^{+0.014}_{-0.033}$ (syst.) | 0.93 |
| 170.0 – 180.0 | $0.720 \pm 0.034$ (stat.) $^{+0.045}_{-0.055}$ (syst.) | 0.91 |
| $x_\gamma^{\text{meas}} < 0.8$ | | |
| 0.0 – 90.0 | $0.0034 \pm 0.0008$ (stat.) $^{+0.0013}_{-0.0007}$ (syst.) | 0.79 |
| 90.0 – 130.0 | $0.0230 \pm 0.0030$ (stat.) $^{+0.0044}_{-0.0014}$ (syst.) | 0.82 |
| 130.0 – 140.0 | $0.070 \pm 0.010$ (stat.) $^{+0.011}_{-0.007}$ (syst.) | 0.84 |
| 140.0 – 150.0 | $0.110 \pm 0.014$ (stat.) $^{+0.009}_{-0.008}$ (syst.) | 0.86 |
| 150.0 – 160.0 | $0.162 \pm 0.015$ (stat.) $^{+0.018}_{-0.009}$ (syst.) | 0.84 |
| 160.0 – 170.0 | $0.187 \pm 0.017$ (stat.) $^{+0.011}_{-0.017}$ (syst.) | 0.82 |
| 170.0 – 180.0 | $0.247 \pm 0.020$ (stat.) $^{+0.016}_{-0.035}$ (syst.) | 0.76 |
| $x_\gamma^{\text{meas}} < 0.7$ | | |
| 0.0 – 90.0 | $0.0023 \pm 0.0006$ (stat.) $^{+0.0010}_{-0.0005}$ (syst.) | 0.75 |
| 90.0 – 130.0 | $0.0168 \pm 0.0027$ (stat.) $^{+0.0051}_{-0.0015}$ (syst.) | 0.78 |
| 130.0 – 140.0 | $0.046 \pm 0.008$ (stat.) $^{+0.006}_{-0.004}$ (syst.) | 0.80 |
| 140.0 – 150.0 | $0.063 \pm 0.012$ (stat.) $^{+0.016}_{-0.005}$ (syst.) | 0.79 |
| 150.0 – 160.0 | $0.104 \pm 0.013$ (stat.) $^{+0.007}_{-0.007}$ (syst.) | 0.77 |
| 160.0 – 170.0 | $0.133 \pm 0.015$ (stat.) $^{+0.008}_{-0.012}$ (syst.) | 0.76 |
| 170.0 – 180.0 | $0.172 \pm 0.017$ (stat.) $^{+0.010}_{-0.026}$ (syst.) | 0.70 |

**Table 7.** Differential cross-section $\frac{d\sigma}{d\Delta \phi}$ for photons accompanied by a jet, and hadronisation correction.
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