1 Introduction

Beauty production measurements provide precision tests of perturbative QCD. At the Tevatron, the total $b\bar{b}$ cross section is about $50 \mu b$, resulting in an event rate of few kHz, thus, in a very high statistics. In the past years, the publication of "controversial" beauty cross section measurements by CDF and DØ in RunI, has led to many developments both in the theoretical calculations beyond NLO and the experimental approach, resulting in a better agreement between data and theory as it is shown in this paper. A major role, concerning theoretical improvements, has been played by the implementation of the so called Fixed-Order with Next-to-Leading-Log (FONLL) calculation. Also, there have been substantial changes in bottom fragmentation function as extracted from experimental data and for the used Parton Distribution Functions (CTEQ6M). On the other hand, from the experimental side, there have been many improvements in the treatment of data inputs, for instance avoiding deconvolution and extrapolation to parton level with Monte Carlo simulations, and implementing the use of real observables as $b$-hadrons and $b$-jets.

2 B hadron production cross section using $J/\psi$

A measurement of the $B$-hadron ($H_b$) production cross section has been performed by CDF, using data corresponding to an integrated luminosity of $39.7 \text{ pb}^{-1}$. First, the inclusive production cross section of $J/\psi$ is measured, considering $J/\psi \rightarrow \mu^+\mu^-$. This cross section contains contributions from various sources, including prompt production of charmonium, decays of excited charmonium states and decays of $B$-hadrons; once the latter $J/\psi$ component is extracted,
it is possible to determine in a very clean way the B-hadron cross section. A di-muon trigger is used to select the events: two oppositely charged muons are required to be reconstructed from tracks measured in the tracking system and matched to track segments detected in the muon chambers. Central muons ($|y| < 0.6$) with $p_T > 1.5$ GeV/c are used: the offline reconstruction efficiency is about 99% independently by the $p_T$, thus the measurement of $J/\psi$ cross section covers all transverse momenta from 0 to 20 GeV/c in the central rapidity range $|y| < 0.6$. To separate prompt $J/\psi$ and $J/\psi$ from decay $H_b \rightarrow J/\psi X$, lifetime distributions are used. B-hadrons have long lifetimes, on the order of picoseconds, so that $J/\psi$ from those decays are usually displaced from the primary vertex, taken as the beam position in the $r-\phi$ plane. The signed projection of the flight distance of $J/\psi$ on its transverse momentum, $L_{xy}$, is, in general, a good measurement of the displaced vertex; nevertheless, to reduce the dependence on the $J/\psi$ $p_T$ bin, the variable $x = L_{xy} \times (M_{J/\psi}/p_{J/\psi})$, called pseudo-proper decay time, is used. A Monte Carlo simulation is implemented to model the $x$ distributions from B-hadron events and, finally, an unbinned maximum likelihood fit is used to extract the B fraction from the data for different ranges in $p_{J/\psi}$. Figure 1 shows an example of fits to the pseudo-proper decay time; the B fraction varies from 10% (low $p_T$) to 45% (high $p_T$). The extracted differential cross section of the B-hadrons over the transverse momentum range from 0 to 25 GeV/c is shown in figure 2. The cross section is corrected for the branching fraction $Br(H_b \rightarrow J/\psi X) = 1.16 \pm 0.10\%$ and $Br(J/\psi \rightarrow \mu^+ \mu^-) = 5.88 \pm 0.10\%$, and divided by two to have the single B-hadron cross section. The most recent theoretical calculations are also superimposed, showing a remarkable agreement with data.

3 B-jet production

The measurement of the inclusive $b$-jet cross section in RunII (CDF), is based on about 300 pb$^{-1}$ of data. The use of jets extends the upper reach of the beauty production measurement performed using exclusive decays ($P_T^{had} < 25$ GeV/c). Besides, theoretical uncertainties on fragmentation are rather small. A cone-based iterative MidPoint algorithm is used for jet reconstruction in the $Y-\phi$ space, using a cone radius of 0.7. Only jets in the central rapidity region ($|y| < 0.7$) are considered. The jet energy scale is corrected, using a Monte Carlo simulation, to compensate for energy losses at calorimeter level.

The analysis exploits the good tracking capabilities of the detector and rely on b-jet identification done by secondary vertex reconstruction. The b-tagging algorithm uses displaced tracks associated with a jet that are within the jet cone. The search for secondary vertices is defined in two steps, with selection based on the significance of the impact parameter and of the decay length $L_{xy}$. The sign of $L_{xy}$ is used as further selection to reject mistagged jets. To determine
the heavy flavour content of a tagged jet, thus to extract the fraction of b-jets, the shape of the secondary vertex mass distribution is used: although a full reconstruction of the hadron invariant mass is not possible, due to the presence of neutral particles and energy lost because of detector resolution, the invariant mass of tracks used to find the secondary vertex constitutes a good discrimination for jets from long-lived b or c hadrons. The mass of secondary vertex depends on jet transverse momentum and the fit is performed considering independently each bin in jet \( P_T \); in figure 3 on the left, mass distribution and fit results are presented for one bin in jet \( P_T \) as example. On the right, the fraction of b-tagged jets as a function of jet \( P_T \) is shown: the total errors and systematic uncertainties are superimposed. Figure 4 shows the inclusive b-jet cross section over a \( P_T \) range between 38 and 400 GeV/c. Statistical and systematic error on the last bins is dominated by the error on b-tagged jets fraction. One of the main systematic error contributions comes from the jet energy scale: a conservative 5\% uncertainty is considered at this stage, although on-going studies show the possibility to reduce it at 3\%. The b-jet cross section is compared with leading order (LO) prevision from Pythia Monte Carlo (CTEQ5L), and results are in agreement with expectation: a NLO and beyond comparison is in progress. DØ is also performing a b-jet cross section measurement using a muon-tagging method to select jet sample enhanced in heavy flavor content: work is in progress to separate the b-jet content from the background.

4 Upsilon production

The DØ experiment has performed a precise measurement of the production of the \( \Upsilon(1S) \) bottomonium state, reconstructed through its decay \( \Upsilon(1S) \rightarrow \mu^+ \mu^- \). The differential cross section as a function of the \( \Upsilon \) transverse momentum is determined in three rapidity ranges,
0 < |y| ≤ 0.6, 0.6 ≤ |y| ≤ 1.2, and 1.2 ≤ |y| ≤ 1.8. The data used in this analysis correspond to 159 pb⁻¹, collected with a scintillator-based di-muon trigger; two opposite-charge muon candidates are required, each of them with \( p_T > 3 \text{ GeV/c} \) and \(|y| < 2.2\), and matched to a track found in the central tracking system. Isolation requirements are imposed to reduce the dominant background from \( b \bar{b} \). Two typical examples of di-muon mass distribution in different bins of rapidity and in the \( p_T \) bin of \( 4 \text{ GeV/c} < p_T^\mu < 6 \text{ GeV/c} \) are showed in Figure 5: the clear \( \Upsilon(1S) \) signal is accompanied by a shoulder from \( \Upsilon(2S) \) and \( \Upsilon(3S) \). The mass distribution fits use three separate mass functions for each of the \( \Upsilon(nS) \) states. The overall systematic errors are about 10%, excluding luminosity uncertainty that is 6.5%: the fitting procedure is one of the main source of uncertainties, while others as momentum resolution, track quality and track matching requirements contribute for less than 2% each. The current analysis assumes the \( \Upsilon(1S) \) produced unpolarized, in agreement with previous CDF results (polarization parameter \( \alpha = -0.12 \pm 0.22 \) for \( 8 < p_T < 20 \text{ GeV/c} \)); thus, contribution to the systematic uncertainties is not included. Differential cross sections, normalized to unity, for the three rapidity ranges, are shown in Figure 6: they are compared to theoretical predictions, that combined separate perturbative approaches for the low and high \( p_T \) regions.

5 Conclusions

Studies of beauty production are important tests for perturbative QCD: results from CDF and DØ benefit from the very high statistic provided by the Tevatron collider and they are generally compatible with the recent theoretical predictions. Further improvements are expected in the near future and new measurements on \( b \bar{b} \) cross section and correlations are already in progress.

References

1. S.Frixione, M.Mangano, Nucl. Phys. B 483 (1997) 321, [hep-ph/9605270]
2. The CDF Collaboration, [hep-ex/0412071], Published in Phys.Rev.D71:032001,2005.
3. CDF Public results in [http://www-cdf.fnal.gov/physics/new/qcd/qcd_plots/bjets_run2/blessed_results.html](http://www-cdf.fnal.gov/physics/new/qcd/qcd_plots/bjets_run2/blessed_results.html)
4. The DØ Collaboration, [hep-ex/0502030], FERMI-LAB-PUB-05/020-E; Submitted to PRL.