Dark Energy Survey Year 1 Results

Citation for published version:
(DES Collaboration) 2019, 'Dark Energy Survey Year 1 Results: Measurement of the Galaxy Angular Power Spectrum', Monthly Notices of the Royal Astronomical Society, vol. 487, no. 3, pp. 3870-3883. https://doi.org/10.1093/mnras/stz1514

Digital Object Identifier (DOI):
10.1093/mnras/stz1514

Link:
Link to publication record in Edinburgh Research Explorer

Published In:
Monthly Notices of the Royal Astronomical Society

General rights
Copyright for the publications made accessible via the Edinburgh Research Explorer is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

Take down policy
The University of Edinburgh has made every reasonable effort to ensure that Edinburgh Research Explorer content complies with UK legislation. If you believe that the public display of this file breaches copyright please contact openaccess@ed.ac.uk providing details, and we will remove access to the work immediately and investigate your claim.
Dark Energy Survey Year 1 Results: Measurement of the Galaxy Angular Power Spectrum

H. Camacho1,2,†, N. Kokron1,2‡, F. Andrade-Oliveira3,4,†, R. Rosenfeld4,2, M. Lima1,2, F. Lacasa5,2, F. Sobreira6,2, L. N. da Costa7,8, S. Avila8, K. C. Chan9,10, M. Crocce9,10, A. J. Ross11, A. Troja4,2, J. Garcia-Bellido12,13, T. M. C. Abbott13, F. B. Abdalla14,15, S. Allam16, J. Annis16, R. A. Bernstein17, E. Bertin18,19, S. L. Bridle20, D. Brooks24, E. Buckley-Geer16, D. L. Burke21,22, A. Carnero Rosell23,7, M. Carrasco Kind23,24, J. Carretero25, F. J. Castander9,10, R. Cawthon26, C. E. Cunha21, C. B. D’Andrea27, J. De Vicente28, S. Desai29, H. T. Diehl16, P. Doel14, J. Estrada16, A. E. Evrard30,31, B. Flaugher16, P. Fosalba9,10, J. Frieman16,26, D. W. Gerdes30,31, T. Giannantonio32,33,34, R. A. Gruendl23,24, J. Gschwend27, G. Gutierrez16, D. L. Hollowood35, K. Honscheid11,36, B. Hoyle37,34, D. J. James38, M. W. G. Johnson24, M. D. Johnson24, S. Kent16,26, D. Kirk14, E. Krause39,40, K. Kuehn41, N. Kuropatkin16, H. Lin16, J. L. Marshall42, R. Miquel33,35, W. J. Percival44,45, A. A. Plazas40, A. K. Roma46, A. Roodman21,22, E. Sanchez28, M. Schubnell31, I. Sevilla-Noarbe28, M. Smith47, R. C. Smith13, M. Soares-Santos48, E. Suchyta49, M. E. C. Swanson24, G. Tarle31, D. Thomas8, D. L. Tucker16, A. R. Walker13, J. Zuntz50

(DES Collaboration)

(affiliations are listed at the end of the paper)
* corresponding author: hcamacho@if.usp.br
‡ corresponding author: nickolas.kokron@usp.br
§ corresponding author: felipe.andrade@linea.gov.br

27 July 2018

ABSTRACT

We use data from the first-year (Y1) observations of the Dark Energy Survey (DES) collaboration to measure the galaxy angular power spectrum, and search for its baryonic acoustic oscillations (BAO) feature using a template-fitting method. We test our methodology in a sample of 1800 DES Y1-like mock catalogs. The angular power spectrum ($C_ℓ$) is measured with the pseudo-$C_ℓ$ method, using pixelized maps constructed from the mock catalogs and the DES mask. The covariance matrix of the $C_ℓ$’s in these tests are also obtained from the mock catalogs. We use templates to model the measured spectra and estimate template parameters firstly from the mock catalogs and the DES mask. Tests are also obtained from the mock catalogs. We use templates to model the measured spectra and estimate template parameters firstly from the mock catalogs and the DES mask. After these tests on mocks, we apply our method to a galaxy sample constructed from DES Y1 data specifically for large scale structure studies. This catalog comprises galaxies within an effective area of 1318 deg$^2$ and redshifts in the range 0.6 < $z$ < 1.0. We fit the observed spectra with our optimized templates, considering models with and without BAO features. We find that the DES Y1 data favors a model with BAO wiggles at the 2.6σ confidence level with a best-fit shift parameter of $α = 1.023 ± 0.047$. However, the goodness-of-fit is somewhat poor, with $χ^2/(dof) = 1.49$. We identify a possible cause of this issue and show that using a theoretical covariance matrix obtained from $C_ℓ$’s that are better adjusted to data results in an improved value of $χ^2/(dof) = 1.36$ which is similar to the value obtained with the real-space analysis. Our results correspond to a measurement of the ratio of the angular diameter distance to the effective redshift of our sample, $z_{\text{eff}} = 0.81$ and the BAO physical scale $r_D(z_{\text{eff}} = 0.81) = 10.65 ± 0.49$, consistent with the main DES BAO findings. This is a companion paper to the main DES BAO article showing the details of the harmonic space analysis.

Key words: galaxy angular power spectrum, cosmological parameters
1 INTRODUCTION

The large-scale distribution of galaxies carries information about the cosmological model that best describes our universe (e.g., Dodelson 2003; Lyth & Liddle 2009). After the great success of maps of the cosmic microwave background (CMB) in providing cosmological information, large galaxy surveys have become one of the major contributors to our understanding of gravity and the ingredients that make up the cosmos. They provide evidence for the consistency of our description for the evolution of the universe from the early CMB epoch to present times.

The distribution of galaxies in the universe carries cosmological information that was imprinted from the era when baryons and photons were tightly coupled. The so-called baryon acoustic oscillation (BAO) feature results from processes that occur up to the baryon drag epoch, and are sensitive in particular to the sound horizon $r_s$ at decoupling.

It is possible to quantify the distribution of galaxies by measuring its 2-point correlation function. One can measure the three-dimensional 2-point galaxy correlation function either in real space or measure its Fourier transform, the power spectrum, in harmonic space. In principle both quantities carry the same information, but in practice they may have different sensitivities to the estimation of cosmological parameters due to, among other effects, different covariance matrices, different response to systematic effects, etc. For instance, gaussian covariance matrices for the power spectrum are diagonal in the full-sky case, whereas for the spatial correlation function significant correlations are expected. Hence performing measurements in both real and Fourier space serves as a consistency check, and may also provide complementary information to tame some of the observational issues.

In galaxy surveys where redshifts are not precisely measured, as is the case with photometric redshifts (photo-z), one actually considers the projected galaxy distribution into redshift bins. In this case what is measured is the angular correlation function in real space ($\text{ACF}$, denoted by $w(\theta)$) and/or the angular power spectrum in harmonic space ($\text{APS}$, denoted by $C_\ell$ in the following).

The APS is studied in the present work, which uses data from the first year (Y1) of observations from the Dark Energy Survey (DES, Flaugher et al. 2005), a large photometric survey in five bands that is planned to cover 5000 deg$^2$ of the sky in a 5-year campaign. The DES uses the Dark Energy Camera (DECam, Flaugher et al. 2015), a 570-Megapixel camera mounted on the 4-meter Blanco telescope at the Cerro Tololo Inter-American Observatory, Chile and is currently in its fifth year of data acquisition. The DECam received its first light in September 2012, followed by a Science Verification (SV) period covering an area of approximately 250 deg$^2$. Measurements of the ACF and the impact of systematic errors in the SV data were reported in Crocce et al. (2016). More recently, cosmological results from combined clustering and weak lensing measurements in the DES Y1 data have been presented (Abbott et al. 2017a).

The BAO feature in the 2-point galaxy correlation function has been observed in several surveys. A few examples are the 2-degree Field Galaxy Redshift Survey (2dFGRS) (Percival et al. 2001; Cole et al. 2005), the Sloan Digital Sky Survey (SDSS) I, II, III and IV (Eisenstein et al. 2005; Padmanabhan et al. 2012; Anderson et al. 2014a; Ross et al. 2015; Alam et al. 2017; Ata et al. 2018) and the WiggleZ survey (Blake et al. 2011). In particular, the BAO scale was measured in SDSS photometric samples using the ACF (Carnero et al. 2012; Sawangwit et al. 2011; de Simoni et al. 2013) and the APS (Blake et al. 2007; Seo et al. 2012).

In this work we use a template-based method to study the BAO feature in the angular power spectra from the DES Y1 data. We describe our method and test it on realistic survey mocks. These mocks were also used to measure the covariance matrix of the $C_\ell$’s. The covariance matrix was then used to find the likelihood corresponding to the template adopted to model the data. We estimate the significance of the detection of the BAO feature for a baseline template using two independent methods: a maximum likelihood estimator (MLE) and a Markov Chain Monte Carlo (MCMC) method. We also present the reduced $\chi^2$ values for the mocks to demonstrate the goodness-of-fit. We explore the robustness of our baseline model to the estimation of parameters testing different choices of settings and assumptions in the analysis. After the validation of our methodology we apply it to Y1 data with the intent to search for BAO features. We find that the DES Y1 data favors a model with BAO wiggles at the 2.6 $\sigma$ confidence level with a best-fit shift parameter of $\alpha = 1.023 \pm 0.047$ with a somewhat large value of $\chi^2/(\text{dof}) = 1.49$. We investigate this issue substituting the covariance matrix obtained from the mocks by a gaussian theoretical covariance matrix taking into account the Y1 mask with input $C_\ell$’s that are better adjusted to data obtaining an improved value of $\chi^2/(\text{dof}) = 1.36$ which is similar to the value obtained with the real-space analysis.

This paper is part of a series related to the detection of the BAO features in Y1 data. It relies on the construction of a catalog suitable for the study of clustering of galaxies, especially concerning the BAO feature (Crocco et al. 2017), the mock catalogs used to validate the analysis and results (Avila et al. 2017) and the computation of galaxy photo-zs (Gaztanaga et al. in prep). Other papers detail methods to study the BAO feature in configuration space with the angular correlation function $w(\theta)$ (Chan et al. 2018), and using the comoving transverse separation (Ross et al. 2017), while the present work details the use of the angular power spectrum. The joint results applied to the Y1 data are described in the BAO main paper (Abbott et al. 2017b).

This paper is organized as follows. We start by describing the theoretical modelling of the angular power spectrum in § 2, including the template used to study the BAO feature. In § 3 we describe the DES Y1 galaxy catalog constructed for BAO studies, focusing on the redshift binning, pixelization and masking. The 1800 mock catalogs used for the verification of our measurements, for the covariance matrix estimation and for testing our parameter estimation from the template method are briefly presented in § 4. In § 5 the measurement of the APS using the pixelized maps is described. The methodology we adopt is tested on the mocks in § 6 where we also study the impact of different choices of templates and settings on the parameter estimation as robustness checks. Having validated our methodology, we apply it for Y1 data in § 7 where we concentrate on finding BAO features in the angular power spectrum. Finally, in § 8 we present our conclusions.
2 THEORY

In this Section we review basic concepts used for the theoretical modelling throughout the paper.

2.1 Angular Power Spectrum and Theoretical Covariance Matrix

We define the 3-dimensional matter overdensity \( \delta_m(\mathbf{x}) \) as

\[
\delta_m(\mathbf{x}) = \frac{\rho_m(\mathbf{x}) - \bar{\rho}_m}{\bar{\rho}_m},
\]

where \( \rho_m(\mathbf{x}) \) is the matter density at point \( \mathbf{x} \) and \( \bar{\rho}_m \) is the background matter density.

We decompose \( \mathbf{x} = \chi(z) \hat{n} \) where \( \hat{n} \) is the angular direction and \( \chi(z) \) is the comoving angular-diameter distance at redshift \( z \). Since we only consider flat-universe cosmologies, \( \chi(z) \) is simply the comoving radial distance to redshift \( z \).

In Fourier space, the overdensity is

\[
\delta_m(\mathbf{k}) = \int d^3x \ e^{-i\mathbf{k} \cdot \mathbf{x}} \delta_m(\mathbf{x}),
\]

and it defines the 3-dimensional matter power spectrum \( P_m(k) \) by the relation

\[
\langle \delta_m(\mathbf{k}) \delta_m(\mathbf{k'}) \rangle = (2\pi)^3 \delta^3(\mathbf{k} - \mathbf{k'}) P_m(k).
\]

On linear scales, we assume that the 3-dimensional galaxy overdensity \( \delta_{gal}(\mathbf{x}) \) is related to the matter overdensity by

\[
\delta_{gal}(\mathbf{x}) = \frac{n_{gal}(\mathbf{x}) - \bar{n}_{gal}}{\bar{n}_{gal}} = b(z) \delta_m(\mathbf{x}),
\]

where \( n_{gal}(\mathbf{x}) \) is the galaxy number density at \( \mathbf{x} \), \( \bar{n}_{gal} \) is its mean value and \( b \) is the scale-independent linear galaxy bias. Therefore one has the relation \( P_m(k) = b^2 P_{gal}(k) \).

For a normalized galaxy selection function \( \phi'(z) = dN/dz \) at photo-z bins \( i \), we define the projected 2-dimensional galaxy overdensity \( \delta_{gal,i}(\hat{n}) \) as

\[
\delta_{gal,i}(\hat{n}) = \int d\phi'(z) \delta_{gal}(\mathbf{x}).
\]

This galaxy overdensity can be decomposed into spherical harmonics \( Y_{lm} \) as

\[
\delta_{gal,i}(\hat{n}) = \sum_{\ell=0}^{\infty} \sum_{m=-\ell}^{\ell} a_{\ell m} Y_{\ell m}(\hat{n}),
\]

where \( a_{\ell m} \) are the harmonic coefficients. The angular cross-spectrum \( C_{ij}^{\ell} \) is defined via

\[
\langle (a_{\ell m})^* (a'_{\ell' m'}) \rangle \equiv \delta_{l\ell m m'} C_{ij}^{\ell},
\]

and the angular power spectrum at \( z \) bin \( i \) is defined by \( C_{ij}^{\ell} \equiv C_{ij}^{\ell}(z) \). One can write the spherical harmonics coefficients as (see e.g. Crocce et al. 2011; Sobreira et al. 2011)

\[
a_{\ell m} = \int d\phi'(z) \int \frac{d^3k}{(2\pi)^3} \delta_{gal}(\mathbf{k},z) 4\pi \mathbf{k} \cdot j_{\ell}(k\chi) Y_{\ell m}(\hat{k}),
\]

where in linear theory \( \delta_{gal}(\mathbf{k},z) = G(z) \delta_{gal}(\mathbf{k},0) \) and \( G(z) \) is the linear growth function normalised such that \( G(0) = 1 \). Hence, from Eqs. (7) and (8) we can write \( C_{ij}^{\ell} \) as:

\[
C_{ij}^{\ell} = \frac{2}{\pi} \int dk \ k^2 P_{gal}(k) \left\{ \Psi_i^j \right\}^2,
\]

where

\[
\Psi_i^j = \int dz \ G(z) \phi'(z) j_{\ell}(k\chi(z)).
\]

A similar symmetrized expression holds for \( C_{ij}^{\ell} \), replacing \( \left\{ \Psi_i^j \right\}^2 \) by \( \Psi_i^j \Psi_j^i \) in Eq. (9).

We include linear redshift space distortions in our fiducial modeling by modifying \( \Psi_i^j \) to:

\[
\Psi_i^j = \int dz \ \beta(z) G(z) \phi'(z) \left\{ \frac{2\ell^2 + 2\ell - 1}{(2\ell + 3)(2\ell - 1)} j_{\ell}(k\chi) - \frac{\ell(\ell - 1) j_{\ell-2}(k\chi)}{(2\ell - 1)(2\ell + 1)} \right\} j_{\ell+2}(k\chi),
\]

where

\[
\beta(z) = \frac{1}{b(z)} \frac{d\ln G}{d\ln a}.
\]

The Gaussian covariance matrix for \( C_{ij}^{\ell} \)'s measured at photo-z bins \( i \) and \( j \) can be theoretically modeled in the so-called \( f_{sky} \) approximation as:

\[
\text{Cov}[\text{APS}]_{ij}^{\ell\ell'} = \langle C_i^{\ell} C_j^{\ell'} \rangle - \langle C_i^{\ell} \rangle \langle C_j^{\ell'} \rangle = \frac{2}{f_{sky} \Delta(2\ell + 1)} \left( \delta_{ij}^{\ell\ell'} + \frac{\delta_{ij}}{\bar{n}_i} \right)^2 \delta_{\ell\ell'},
\]

where \( \Delta \) is the bin size, \( f_{sky} \) is the sky fraction covered by the survey, \( \bar{n}_i \) is the mean galaxy number density at bin \( i \) and \( \delta_{ij} \) is a Kronecker delta.

The analytical expression we actually use to estimate the theoretical covariance is more realistic, as it is tied to the pseudo-\( C_{ij}^{\ell} \) estimator (see § 5) and corrects for binning and mask effects (Efstathiou 2004). Interestingly, we find that the above approximation multiplied by a boost factor agrees well with the full covariance expression and with the covariance estimated from mock catalogs in the range of \( \ell \) explored in this work (see § 6.2).

2.2 \( C_{ij}^{\ell} \) Template

Our goal is to extract from mocks and from DES Y1 observations the scale associated with the BAO feature, namely the angular distance scale \( D_A(z) \). In order to be as insensitive as possible to nonlinear effects such as bias and redshift space distortions, we will use a template method (Seo et al. 2012; Anderson et al. 2014b; Gil-Marín et al. 2016; Ata et al. 2018; Ross et al. 2017; Chan et al. 2018).

Since the selection function for the simulations and data is fully specified, the \( C_{ij}^{\ell} \) template may be defined by first settling on a template for \( P(k) \) and projecting onto \( C_{ij}^{\ell} \)’s using Eq. (9). We start with

\[
P_{\text{temp}}(k) = [P(k)^{\text{lin}} - P^{\text{nw}}(k)] e^{-k^2 \Sigma_{\text{nl}}^2} + P^{\text{nw}}(k),
\]

where \( P(k)^{\text{lin}} \) is the linear power spectrum and the no-wiggle power spectrum \( P^{\text{nw}}(k) \) is obtained from the Eisenstein-Hu parametrization (Eisenstein & Hu 1998). The nonlinear damping scale is fixed at \( \Sigma_{\text{nl}} = 5.2 \) Mpc/h, which was determined from a fit to the mean of mocks (Chan et al. 2018).

We chose our template by optimizing the BAO signal in the mock catalogs. Tests of different templates will be shown below. Our default template for \( C_{ij}^{\ell} \) is given by:

\[
C(\ell) = B_0 C^{\text{temp}}(\ell/\alpha) + A_0 + A_1 \ell + A_2 / \ell^2,
\]
where $C^{temp}(l)$ is the projection of $P^{temp}(k)$ as described above. The amplitude $B_0$ is related to the linear bias squared and the parameters $A_i$ take into account scale-dependent bias, shot noise, uncertainties in the redshift-space distortions, etc. We allow these parameters to change with redshift. Therefore, for 4 redshift bins we will have 16 of these parameters to adjust. We will marginalize over them in MCMC analysis and keep them fixed at the values that maximize the likelihood in the MLE analysis as will be described in section 6.

The most important parameter in our analysis is the so-called shift parameter $\alpha$, which measures the shift of the BAO peak positions with respect to a fiducial cosmology. We will assume that it does not change significantly with respect to its value at the “effective redshift” of the sample used ($z_{eff} = 0.81$ in the BAO Y1 sample) (Abbott et al. 2017a). If the fiducial cosmology used to compute $P(k)^{lin}$ and $P(k)^{nw}$ turns out to be the correct one then one should find $\alpha = 1$. The shift parameter is related to the change in the BAO location, given by the ratio of the angular diameter distance $D_A(z)$ to the sound horizon scale at the drag epoch ($r_d$):

$$\alpha = \frac{(D_A(z)/r_d)}{(D_A(z)/r_d)_{fid}}. \quad (16)$$

For example, for a fiducial cosmology given by the MICE simulations ($h = 0.7$, $\Omega_m = 0.25$, $\Omega_\Lambda = 0.75$) (Crocce et al. 2010; Fosalba et al. 2015b) we find that, with respect to the cosmology found by DES combined with other observations ($h = 0.678$, $\Omega_m = 0.30$, $\Omega_\Lambda = 0.70$) (Abbott et al. 2017b), $\alpha \approx 1.03$.

We will test this parametrization with the mocks below and show that it results in biases below 1% for the parameter estimation. We study the impact of other templates as robustness tests in § 6.

### 3 DES Y1 GALAXY CATALOG

#### 3.1 Catalog

The catalog for LSS analyses using DES Y1 data was created from the so-called Y1 Gold catalog (Dricala-Wagner et al. 2018) which in turn was built from the data reduction performed by the Dark Energy Survey Data Management (DESDM) system on DECam images. The LSS sample selection is based on color, magnitude and redshift cut designed to provide an optimal balance between the density of objects and the photometric redshift uncertainty for $z > 0.6$, minimizing the forecasted BAO error (Crocce et al. 2017). We will use the LSS catalog with photometric redshifts obtained with a Multi-Object Fitting (MOF) photometry (Dricala-Wagner et al. 2018) and the Directional Neighborhood Fitting (DNF) algorithm (De Vicente et al. 2016). After proper masking described in (Crocce et al. 2017) the catalog has approximately 1.3 million galaxies in an area of 1317 deg$^2$.

We divide the catalog into 4 tomographic photo-z bins with width $\Delta z_{phot} = 0.1$ in the range $0.6 < z_{phot} < 1.0$. In Fig. 1 we show the redshift distribution for each bin obtained by stacking a Monte Carlo sampled value of the photo-z from the estimated probability distribution function for each object. The bins are defined using a point-estimate of the photo-z given by the maximum likelihood redshift produced by DNF.

The LSS catalog also comes with a correction for the three main systematic dependencies found on observational quantities: local stellar density, mean i-band PSF (FWHM) and detection limit (g-band depth). These corrections are encapsulated in a weight factor for each object, which is applied to reduce these dependencies.

#### 3.2 Pixelized map generation

Each redshift bin is pixelized using HEALPix (Gorski et al. 2005) at a resolution of $N_{\text{side}} = 1024$, with $N_I$ galaxies in each pixel $I$. A pixelized angular mask described in (Crocce et al. 2017) is used to find the density contrast maps. Each pixel in the mask comes with its fractional coverage which we denote $w_I$ such that

$$\frac{\sum I w_I}{N_{\text{pix}}} = f_{\text{sky}}, \quad (17)$$

where $N_{\text{pix}} = 12N_{\text{side}}^2$ is the total number of pixels for a given resolution and again $f_{\text{sky}}$ is the survey sky fraction.

We degrade the mask resolution from $N_{\text{side}} = 4096$ to $N_{\text{side}} = 1024$ keeping the fractional coverage as an average of the smaller pixels contained in the large (smaller resolution) pixel. The number density of galaxies $n_I$ in each pixel inside the footprint is computed as:

$$n_I = \frac{N_I}{w_I \Omega}, \quad (18)$$

where $\Omega$ is the (common) area of one pixel. The average number density of galaxies is

$$\bar{n} = \frac{\sum_I N_I}{\left(\sum_I w_I \Omega\right)} \Omega. \quad (19)$$
and finally the density contrast $\delta_l$ in each pixel is given by:

$$\delta_l = \frac{n_l}{n} - 1. \quad (20)$$

These maps generated for each redshift bin are used to measure the APS as explained in § 5.

4 DES MOCK SIMULATIONS

In addition to the DES Y1 galaxy catalog, we use a set of 1800 galaxy mock simulations, especially made for studies of large-scale structure in DES, including the present BAO analysis (Avila et al. 2017).

These mocks serve a dual purpose in our study. First, we use them to test our codes for estimating $C\ell$’s, covariances and the BAO feature extraction in a DES-like survey. Second, we make direct use of the covariance matrices estimated from them in the BAO analysis of the DES Y1 data.

These simulations match all aspects of the DES Y1 data, including its footprint, abundance and clustering of galaxies and redshift distribution. One starts with halo catalogs that are constructed with the HALOGEN method (Avila et al. 2015), such that they satisfy halo mass-functions and bias appropriately from N-body simulations. Next, galaxies are assigned to these halos according to a hybrid Halo Occupation Distribution (HOD)/Halo Abundance Matching (HAM) prescription. The methodology is much faster than using full N-body simulations and allows for the construction of thousands of simulations. These mock catalogs were constructed using the MICE Grand Challenge N-body simulations (Crocce et al. 2010; Fosalba et al. 2015b; Crocce et al. 2015; Fosalba et al. 2015a), with cosmological parameters close but not equal to those of the Planck mission. We refer the reader to Avila et al. (2017) for details of the construction of these DES galaxy mocks.

5 ANGULAR POWER SPECTRUM MEASUREMENT IN CUT SKY

For data collected over the whole sky, an unbiased estimator of the APS is simply the average of the $a_{\ell m}$ coefficients over all $m$ values (Hivon et al. 2002):

$$\bar{C}_\ell = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{m=\ell} |a_{\ell m}|^2. \quad (21)$$

When performing full-sky estimations, we compute the coefficients $a_{\ell m}$ from the pixelized density contrast maps using the anafast routine within HEALPIX.

As the DES measurements are not made over the full-sky, the previous estimator is not appropriate, since spherical harmonics no longer provide a complete orthonormal basis to expand angular overdensities. In this case, we use the so-called pseudo-$C\ell$ method to relate the APS measured in a masked sky $\bar{C}_\ell$ to the “true” APS $C\ell$ (Hivon et al. 2002). The pseudo-$C\ell$ estimator relies on the assumption:

$$\langle \tilde{C}_\ell (\delta_{gal}(\mathbf{n})) \rangle = \sum_{\ell'} \mathcal{M}_{\ell \ell'} C_{\ell'} (\delta_{gal}(\mathbf{n})), \quad (22)$$

where $\mathcal{M}$ is called the coupling matrix. In the equation above the masked density contrast field $\tilde{\delta}_{gal}$ is related to the full-sky one $\delta_{gal}$ by a mask function $M$:

$$\tilde{\delta}_{gal}(\mathbf{n}) = M(\mathbf{n}) \delta_{gal}(\mathbf{n}). \quad (23)$$

It can be shown that the coupling matrix in terms of Wigner 3 - j symbols is given by:

$${\mathcal{M}}_{\ell_1\ell_2} = (2\ell_2 + 1) \sum_{\ell_3} \frac{2\ell_3 + 1}{4\pi} C_{\ell_3}(M) \begin{pmatrix} \ell_1 & \ell_2 & \ell_3 \\ 0 & 0 & 0 \end{pmatrix}^2, \quad (24)$$

where $C_{\ell}(M)$ is the angular power spectrum of the pixelized mask. Notice that for full sky measurements, $\mathcal{M}_{\ell\ell'}$ is simply the identity matrix and in general it carries information about the survey geometry and mask. The true $C_\ell$ can then be estimated from the pseudo-$C_\ell$ by solving the linear system defined by Eq. (22).

We use two independent codes to measure $C_\ell$’s via the pseudo-$C_\ell$ method without shot-noise subtraction. The first code is our own implementation of the pseudo-$C_\ell$ method in python. The second is the publicly available code NaMaster\footnote{https://github.com/damonge/NaMaster}, which is implemented in C. We compared the $C_\ell$’s estimated from the two codes when applied to a single DES mock simulation. The two codes agree at better than 5% for all $\ell$ values considered here, and better than 1% for $\ell > 100$, indicating our measurements are robust. All results presented in the remainder of the paper will make use only of the NaMaster code.

We consider in our default analysis multipoles in the range $30 < \ell < 330$, corresponding roughly to the angular scales used in the $w(\theta)$ analysis (Chan et al. 2018), and we then bin using a bin width of $\Delta\ell = 15$ in order to make the reduced covariance matrix more diagonal and amenable to algebraic manipulations. Effects of different ranges and binnings will be studied as robustness tests in § 6.4.

Finally, the covariance matrix is estimated from the $N_m = 1800$ mocks as:

$$\text{Cov}[\text{APS}]_{\ell\ell'} = \frac{1}{N_m - 1} \sum_{k=1}^{N_m} \left( C_{\ell}'(k) - \bar{C}_{\ell}' \right) \left( C_{\ell'}'(k) - \bar{C}_{\ell'}' \right), \quad (25)$$

where the average $\bar{C}_{\ell}'$ at photo-z bin $i$ is given by

$$\bar{C}_{\ell}' = \frac{1}{N_m} \sum_{k=1}^{N_m} C_{\ell}'(k). \quad (26)$$

6 TESTS OF METHODOLOGY ON MOCKS

We now apply our full methodology on the 1800 DES Y1 HALOGEN mock simulations with known cosmology and perform robustness tests to estimate the impact of changing our default settings on parameter estimation.

6.1 Measurements of the APS

In Fig. 2 we show the results of our $C_\ell$ measurements in the four photo-z bins for the 1800 mocks together with the mean of the mocks. We also show theoretical predictions from $C_\ell$'s.
Figure 2. Measurements of $C_\ell$ in four photo-z bins for the 1800 mocks (gray lines) and the Y1 data (red circles). Dashed line shows the theoretical prediction from a linear spectrum with MICE cosmology multiplied by a bias factor (shown in the panels) and including shot-noise and shaded regions show 68% and 95% C.L. from mocks measurements. The blue line is the average of the mocks. The $\chi^2$ values show reasonable agreement between average measurements of the mocks and measurements on data.

computed with a linear matter spectrum at the same cosmology as the mocks. In each photo-z bin, we multiply the theoretical matter $C_\ell$’s by a galaxy bias factor squared determined by (Avila et al. 2017) and add a shot-noise determined by the number density of Y1 galaxies in that photo-z bin.

The measured $C_\ell$’s from the mocks are in good agreement with the theoretical prediction. However, when compared to data there is some discrepancy in the second and third redshift bins, reflected in the somewhat high value of $\chi^2 = 1.92$ and 1.57 respectively. In these bins the $C_\ell$’s from data exceed the ones from the mocks at large $\ell$’s. We will discuss some consequences of this behaviour below.

6.2 Covariance matrix

In order to quantify the correlation between bandpowers in our analysis, we show the correlation matrix,

$\text{Cov}_{\ell a, \ell b} = \frac{\text{Cov}_{\ell a} \times \text{Cov}_{\ell b}}{\sqrt{\text{Cov}_{\ell a} \times \text{Cov}_{\ell b}}}$, \hspace{1cm} (27)

where the $a, b$ indexes label bandpowers, as measured from the mocks in the left panel of Fig. 3 for the four redshift bins and using our fiducial $\Delta \ell = 15$ binning. We see it is close to block-diagonal with structure similar to the one found in Chan et al. (2018) for the covariance matrix for $w(\theta)$. The right panel of Fig. 3 shows the theoretical estimation for the covariance computed at the mock cosmology, using the mock bias, adding the data shot-noise and correcting for binning and mask effects (Efstathiou 2004). The theoretical covariance is much less noisy, as expected.

In Fig. 4, we compare the diagonal errors of the $C_\ell$’s estimated from the mock simulations and the Gaussian prediction of the fiducial cosmology using two approximations: the naive $f_{\text{sky}}$ approximation Eq. (13) and the prediction of the covariance matrix of the pseudo-$C_\ell$ estimator (Efstathiou 2004; Brown et al. 2005). We find good agreement between the errors coming from the simulation covariance matrix and from the pseudo-$C_\ell$ estimator. However, for the $f_{\text{sky}}$ approximation we find that a “boost factor” of 1.35 is necessary to match the measured errors. This was also the case for a similar analysis in SDSS (Ho et al. 2012).

We will use the full covariance matrix estimated from the mocks. It is well known that statistical noise on the estimation of the covariance matrix from mock realizations translates into a bias on its inverse, the precision matrix, which is the actual fundamental piece on the likelihood estimation. We included this correction factor in our analysis (Hartlap et al. 2007; Dodelson & Schneider 2013; Percival et al. 2014). Given the number of mocks used, we have checked that the correction factor for the precision matrix is always less than 5%, having no impact on the recovered value of $\alpha$.

6.3 Parameter estimation

We use two independent methods for the parameter estimation: a Markov Chain Monte Carlo (MCMC) implemented with encee (Foreman-Mackey et al. 2013) and a maximum likelihood estimator (MLE) with analytical least square fit of the nuisance parameters (Cowan 1998). We used our default BAO template described in § 2.2 with the covariance matrix estimated from the mocks. We performed a joint fit for the 4 photo-z bins with 17 parameters in our default template. In Fig. 5 we show the distribution of $\alpha$ values resulting from fits of our $C_\ell$ measurements in four photo-z bins for the 1800 mocks. The remaining 16 parameters are marginalized over for the MCMC analysis and fixed to the values that maximize the likelihood for the MLE analysis as described in Chan et al. (2018). For the MLE method we find the best fit analytically over the 12 parameters $A_0, A_1, A_2$ in each redshift bin and numerically over the 4 $B_0$’s requiring $B_0 > 0$ for each value of $\alpha$, following Chan et al. (2018) .

For the MCMC we used the flat priors $\alpha \in [0.8, 1.2]$, $A_1 \in [-800, 800] \times 10^{10}$, $A_2 \in [-50, 50] \times 10^8$, $A_3 \in [-200, 200] \times 10^5$ and $B_0 \in (0, 0.6)$. We exclude outliers defined as mocks whose $1\sigma$ values for $\alpha$ lie outside the range $0.8 < \alpha < 1.2$ (see Chan et al. (2018)) using the MLE method. For our fiducial analysis 86.4% of the mocks are kept.

Since our fiducial model has the same cosmology as the mocks we expect to find $\alpha = 1$. In fact we find that the mean value in the mocks is $\bar{\alpha} = 1.006$ for MLE and $\bar{\alpha} = 0.992$ for MCMC. Therefore both our methods recover $\alpha$ with a bias at the subpercent level.

In Fig. 6 we show the results from the MCMC chains when fitting the BAO template to the averaged $C_\ell$ measured in the mock simulations for our fiducial template. In this case, we find for the shift parameter $\alpha = 0.988 \pm 0.060$ and it can be seen that it does not show strong correlations with the nuisance parameters. In fact, the nuisance parameters are poorly constrained, having broad distributions. The best-fit values for $B_0$ and $A_0$ are found to be roughly consistent with the squared bias and the shot-noise in each bin, respectively. For the MLE method we find $\alpha = 1.009 \pm 0.056$ from a fit to the average of the mocks.
Figure 3. $C_\ell$’s correlation matrix for the 4 photo-$z$ bins. Left: measured from the 1800 mock simulations mimicking the DES Y1 data. Right: Theoretical estimation computed at the mock cosmology and accounting for binning and mask effects.

Figure 4. Comparison of the $C_\ell$’s diagonal errors in 4 photo-$z$ bins. For each bin, the top panel shows the standard deviation estimated from the 1800 DES mock simulations (open circles) the Gaussian prediction on the fiducial cosmology (solid lines) after rescaled by an empirical boost factor of 1.35 and the Gaussian prediction from the pseudo-$C_\ell$ method (open triangles). The bottom panels show the relative differences with respect to the mocks standard deviation.

In Fig. 7 we show $C_\ell$’s measured in four photo-$z$ bins for the DES mock simulations. The errors are computed from the mock covariance matrix. The solid line displays the best-fit theoretical prediction using the BAO template described in § 2.2. We see that our BAO template is able to accurately capture the behaviour of the $C_\ell$’s from the mocks.

The compatibility between the two independent methods (MCMC and MLE) is shown in Fig. 8 where we plot the normalized likelihood for the $\alpha$ parameter determined from the average of the mocks for both methods.

In Fig. 9 we show the distribution of $\chi^2$ for the 1800 mocks demonstrating the good fit of our template. Also shown in the plot as a dashed line is the $\chi^2$ obtained from the data using the covariance matrix estimated from the mocks (discussed in § 7).

We estimate the significance of recovering $\alpha$ (or detecting the BAO feature) by measuring the difference in $\chi^2$ as a function of $\alpha$ between a model with no BAO feature (a no-wiggle model), which is independent of $\alpha$, and our BAO template. In Fig. 10 we show $\Delta \chi^2 = \chi^2(\alpha) - \chi^2_{\text{min}}$ for fits of the average $C_\ell$’s from the mocks as a function of the $\alpha$ parameter. The best-fit value is $\alpha_{\text{min}} = 1.009$. From Fig. 10 we see that for the average of the mocks a BAO signal would be detected at $2.3\sigma$ with respect to a no-wiggle model.

We will use the methods described in this section to...
6.4 Robustness Tests

For our default analysis above, a number of choices were made: the binning of harmonics in $\Delta \ell = 15$, adopting study the BAO signal in Y1 data. But before doing so, we use the mocks to perform some robustness tests related to choices made in our analysis.
\[ \Delta \chi^2 = \chi^2(\alpha) - \chi^2_{\text{min}}, \] as a function of \( \alpha \) for the BAO template fitted on the mean of mocks. For each value of \( \alpha \) we subtract from \( \chi^2 \) the value of \( \chi^2_{\text{min}} = \chi^2(\alpha_{\text{min}}) \). Dashed line is the approximately constant \( \chi^2 \) for the non-wiggle template subtracted from the minimum of the template.

In addition to the tests in Table 1, we have also investigated other choices made. These included i) using the Limber approximation (Limber 1953) instead of the full integral calculation in Eqs. (9) and (11), ii) exclusion of linear RSD effects, i.e., using Eq. (10) instead of Eq. (11), iii) exclusion of cross-correlations between photo-z bins in the covariance matrix, iv) use of the theoretical covariance instead of the covariance measured in mocks and v) inclusion of the non-linear matter power spectrum in the \( C_\ell \) modeling. All these tests led to very similar results as the fiducial analysis for \( \alpha \).

Notice that i) and v) affect only small scales, ii) affects only large scales. Meanwhile we expect iii) and iv) to have small effects given that redshift cross-correlations are small for our photo-z bin size and the theoretical covariance matches that measured in the mocks quite well (see § 6.2). Our \( C_\ell \) template has enough flexibility to account for these effects in case they are either included or neglected. Indeed we find that the best-fit template parameters change significantly between one case and another, but the best-fit for \( \alpha \) and the BAO detection significance remain nearly the same.

### 7 BAO IN DES Y1 DATA

We now apply the methods described and tested above to study the BAO feature in the angular power spectrum in the DES Y1 data. In Fig. 11 we show \( C_\ell \)'s measured in four photo-z bins for the DES Y1 data. The errors are computed from the variance of the 1800 mock simulations. The solid line displays the best-fit theoretical prediction using the BAO template described in § 2.

In Fig. 12 we show the \( \Delta \chi^2 = \chi^2(\alpha) - \chi^2_{\text{min}} \) as a function of \( \alpha \) for the DES Y1 data from the MLE described above and also used in Chan et al. (2018). We find \( \alpha = 1.023 \pm 0.047 \) with \( \chi^2_{\text{min}}/\text{dof} = 93.7/63 = 1.49 \). This somewhat large value of \( \chi^2 \) seems to indicate that the covariance matrix obtained from the mocks may underestimate the errors. We will discuss this possibility below.

The small deviation of \( \alpha \) from unity can be traced to the fact that the template cosmology has been fixed to reflect that of the mock simulations (to be consistent with the fact that we also use the covariance from the mock simulations). The mocks have a cosmology slightly different from e.g. the Planck cosmology, and the latter has been shown to be consistent with clustering measurements of the DES Y1 data (Gruen et al. 2018; Abbott et al. 2017b). A difference of a few percent from unity is expected and is also found in a similar analysis in configuration space (Chan et al. 2018; Abbott et al. 2017a). We have repeated our analysis with the covariance matrix re-calculated at the best fit cosmology, and we have not found significant changes in our results, which was also the case for Abbott et al. (2017b).
The fiducial case we adopt has a template \( A_0 + A_1 \ell + A_2 \ell^{-2} \) and \( \Delta \ell = 15, 30 \) \( < \ell < 330 \). When this new covariance matrix is used to fit the \( \alpha \) and the fraction of detected mocks. The fiducial case we adopt has a template \( A_0 + A_1 \ell + A_2 \ell^{-2} \) and \( \Delta \ell = 15, 30 \) \( < \ell < 330 \) shown in boldface.

| case | \( \langle \alpha \rangle \) | \( \langle \sigma \rangle \) | \( S_\alpha \) | \( f(N_{\text{data}}) \) | mean of mocks |
|------|----------------|------------|--------|----------------|----------------|
| \( \Delta \ell = 15, 30 \) \( < \ell < 330 \) : | \( A_0 + A_1 \ell + A_2 \ell^{-1} \) | 1.003 | 0.051 | 0.058 | 0.752 | 1.008 \( \pm \) 0.056 |
| \( A_0 + A_1 \ell + A_2 \ell^{-2} \) | 1.007 | 0.058 | 0.053 | 0.864 | 1.009 \( \pm \) 0.056 |
| \( A_0 + A_1 \ell + A_2 \ell^{-2} \) | 1.011 | 0.056 | 0.055 | 0.851 | 1.013 \( \pm \) 0.056 |
| \( \Delta \ell = 20, 40 \) \( < \ell < 300 \) : | \( A_0 + A_1 \ell + A_2 \ell^{-1} \) | 1.003 | 0.051 | 0.060 | 0.734 | 1.006 \( \pm \) 0.056 |
| \( A_0 + A_1 \ell + A_2 \ell^{-2} \) | 1.006 | 0.059 | 0.056 | 0.812 | 1.006 \( \pm \) 0.058 |
| \( A_0 + A_1 \ell + A_2 \ell^{-2} \) | 1.009 | 0.057 | 0.057 | 0.790 | 1.012 \( \pm \) 0.057 |
| \( \Delta \ell = 15, 45 \) \( < \ell < 330 \) : | \( A_0 + A_1 \ell + A_2 \ell^{-1} \) | 1.004 | 0.050 | 0.059 | 0.736 | 1.009 \( \pm \) 0.056 |
| \( A_0 + A_1 \ell + A_2 \ell^{-2} \) | 1.007 | 0.057 | 0.054 | 0.841 | 1.009 \( \pm \) 0.056 |
| \( A_0 + A_1 \ell + A_2 \ell^{-2} \) | 1.011 | 0.056 | 0.055 | 0.839 | 1.013 \( \pm \) 0.056 |
| \( \Delta \ell = 20, 40 \) \( < \ell < 320 \) : | \( A_0 + A_1 \ell + A_2 \ell^{-1} \) | 1.004 | 0.050 | 0.060 | 0.731 | 1.008 \( \pm \) 0.056 |
| \( A_0 + A_1 \ell + A_2 \ell^{-2} \) | 1.007 | 0.058 | 0.055 | 0.833 | 1.008 \( \pm \) 0.057 |
| \( A_0 + A_1 \ell + A_2 \ell^{-2} \) | 1.011 | 0.056 | 0.057 | 0.831 | 1.014 \( \pm \) 0.057 |

Table 1. Summary of the robustness tests performed on the 1800 mocks using MLE. We show the average values of \( \alpha \) and its 1\( \sigma \) standard deviation for all the mocks, the standard deviation of \( \alpha \) obtained only for the detected mocks \( S_\alpha \) and the fraction of detected mocks. The fiducial case we adopt has a template \( A_0 + A_1 \ell + A_2 \ell^{-2} \) and \( \Delta \ell = 15, 30 \) \( < \ell < 330 \) shown in boldface.

![Figure 12. \( \Delta \chi^2 \) as a function of \( \alpha \) for the DES Y1 galaxy data, when fitted to a BAO templates (solid blue curve) and to a no-wiggle template (dashed black curve).](image1)

![Figure 13. \( \Delta \chi^2 \) as a function of \( \alpha \) for the DES Y1 galaxy data, when fitted using a new theoretical covariance matrix to a BAO template (solid blue curve) and to a no-wiggle template (dashed black curve).](image2)

Finally, we also show the difference in \( \chi^2 \) from our best-fit template and a no-wiggle model. Assuming Gaussian statistics for the likelihood, we find that the angular power spectrum measured from DES Y1 data finds the BAO feature at a significance of 2.6\( \sigma \) level with respect to a no-wiggle template.

In order to address the issue of the large value of \( \chi^2 \) obtained above we study the changes that arise from using a theoretical covariance matrix more well adjusted to the data. We modify the theoretical modelling of \( C_\ell \) used to fit the average of the mocks in Fig. 2 by adding a term proportional to \( \ell \) and fit its coefficient to best reproduce the data. This theoretical \( C_\ell \) is then input in NaMaster to compute a new gaussian covariance matrix that takes into account the Y1 mask and the binning in \( \ell \). When this new covariance matrix is used the minimum \( \chi^2 \) is indeed reduced to \( \chi^2_{\text{min}}/\text{dof} = 85.8/63 = 1.36 \) without a significant change in the estimated value of \( \alpha \), which is found to be \( \alpha = 1.039 \pm 0.053 \) in this case.

In Fig. 13 we show the result of the significance using this new theoretical covariance matrix. The value of \( \alpha \) changed by a third of the standard deviation and the error increased by 13%. Although the changes are small they point to the uncertainties inherent in this analysis.
8 CONCLUSIONS

The DES is on its way to produce the largest survey to date, projected to map 300 million galaxies using photometric techniques in an area of 5000 deg$^2$ up to a redshift $z \approx 1.3$. The Y1 data has been recently analysed resulting in a key paper combining three correlations: weak gravitational lensing, galaxy clustering and their cross-correlation or galaxy-galaxy lensing (Abbott et al. 2017b). Several papers dealing with the essential developments that led to the key paper were also produced (Cawthon et al. 2017; Avila et al. 2017; Davis et al. 2017; Gatti et al. 2017; Hoyle et al. 2018; Drlica-Wagner et al. 2018; Krause et al. 2017).

The work presented here is part of a series of papers mentioned in the Introduction dedicated to searching specifically for the BAO feature in Y1 data. Here we concentrated on the detection of the BAO feature in the angular power spectrum.

We developed a methodology based on template-fitting and tested it on realistic DES Y1 galaxy mocks. First we tested two independent codes for pseudo-$C_l$ estimators and found agreement between codes to better than 1% in nearly all scales of interest. We then measured the APS in four photo-$z$ bins for 1800 mock catalogs, checking their consistency with theoretical expectations. We measured the covariance matrix from the mocks and compared it with a theoretical prediction, finding again good agreement. We then used two independent methods, a maximum likelihood estimator (MLE) and a Markov Chain Monte Carlo (MCMC) analysis to estimate the shift parameter for the average of the mocks and found the two methods to be compatible. Comparing the values of $\chi^2$ for our BAO template to a no-wiggle model we find a $2.3\sigma$ signal for BAO in the mocks.

Several choices were made for our fiducial analysis and we performed a number of robustness tests to assess their impact on the results. We find that our results on the mocks were not significantly sensitive to changing the binning $\Delta \ell$ from 10 to 20, changing the smallest scales of our analysis from $\ell_{\text{max}} = 300$ to $\ell_{\text{max}} = 330$, neglecting the redshift cross-covariance, using the Limber approximation, neglecting linear RSD’s, including a non-linear matter power spectrum and modifying the $C_l$ template used.

We then applied the fiducial analysis to measure the APS of a galaxy sample obtained from DES Y1 data also split into four photo-$z$ bins up to $z = 1$ (Crocce et al. 2017). We obtain a best-fit $\alpha = 1.023 \pm 0.047$. This corresponds to a measurement of the ratio of the angular diameter distance to the effective redshift of our sample $(z_{\text{eff}} = 0.81)$ and the BAO physical scale $r_d$ of $D_A(z_{\text{eff}} = 0.81)/r_d = 10.65 \pm 0.49$. Comparing to the best-fit no-wiggle template we find a significance of $2.6\sigma$ for BAO detection.

This best fit has a somewhat large $\chi^2/\text{(dof)} = 1.49$ value. We could trace the reason to the covariance matrix computed from the mocks, since the $C_l$‘s measured from them seem to underestimate the data at high $\ell$‘s in two redshift bins. We investigate this issue with a new Gaussian theoretical covariance matrix obtained from $C_l$‘s that are better adjusted to the data, taking into account the mask and the binning. With this new covariance matrix we obtain a reduced value $\chi^2 = 1.36$ without significant changes in the recovered value of $\alpha$.

Our results are consistent with those from the real-space BAO analysis of Y1 data (Abbott et al. 2017b) but the methodological uncertainties we found, despite being small, must be understood in more detail in future DES analyses.

The use of photometric data such as that from DES allows us to extend the BAO detection to high-redshift galaxies and the consistency of the BAO scale inferred from CMB and galaxies is an important test of the standard cosmological model over most of the cosmic history. As DES continues to collect and analyze more data, the significance of the BAO feature detection will continue to improve. Data collected over three years of observations (Y3) covers nearly the whole DES footprint. In combination with additional probes of geometry and structure growth, the BAO feature detected in this extended area of DES will be an important element for constraining and distinguishing models of cosmic acceleration in the near future.

ACKNOWLEDGMENTS

HC is supported by CNPq under grant number 141935/2014-6. ML and RR are partially supported by FAPESP and CNPq. AT is supported by FAPESP. We thank the support of the Instituto Nacional de Ciência e Tecnologia (INCT) e-Universe (CNPq grant 465376/2014-2).

We are grateful for the extraordinary contributions of our CTIO colleagues and the DECam Construction, Commissioning and Science Verification teams in achieving the excellent instrument and telescope conditions that have made this work possible. The success of this project also relies critically on the expertise and dedication of the DES Data Management group.

Funding for the DES Projects has been provided by the U.S. Department of Energy, the U.S. National Science Foundation, the Ministry of Science and Education of Spain, the Science and Technology Facilities Council of the United Kingdom, the Higher Education Funding Council for England, the National Center for Supercomputing Applications at the University of Illinois at Urbana-Champaign, the Kavli Institute of Cosmological Physics at the University of Chicago, the Center for Cosmology and Astro-Particle Physics at the Ohio State University, the Mitchell Institute for Fundamental Physics and Astronomy at Texas A&M University, Financiadora de Estudos e Projetos, Fundação Carlos Chagas Filho de Amparo à Pesquisa do Estado do Rio de Janeiro, Conselho Nacional de Desenvolvimento Científico e Tecnológico and the Ministério da Ciência, Tecnologia e Inovação, the Deutsche Forschungsgemeinschaft and the Collaborating Institutions in the Dark Energy Survey.

The Collaborating Institutions are Argonne National Laboratory, the University of California at Santa Cruz, the University of Cambridge, Centro de Investigaciones Energéticas, Medioambientales y Tecnológicas-Madrid, the University of Chicago, University College London, the DES-Brazil Consortium, the University of Edinburgh, the Eidgenössische Technische Hochschule (ETH) Zürich, Fermi National Accelerator Laboratory, the University of Illinois at Urbana-Champaign, the Institut de Ciències de l’Espai (IEEC/CSIC), the Institut de Física d’Altes Energies, Lawrence Berkeley National Laboratory, the Ludwig-
Maximilians Universität München and the associated Excellence Cluster Universe, the University of Michigan, the National Optical Astronomy Observatory, the University of Nottingham, The Ohio State University, the University of Pennsylvania, the University of Portsmouth, SLAC National Accelerator Laboratory, Stanford University, the University of Sussex, Texas A&M University, and the OjDES Membership Consortium.

Based on part on observations at Cerro Tololo Inter-American Observatory, National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy (AURA) under a cooperative agreement with the National Science Foundation. The DES data management system is supported by the National Science Foundation under Grant Numbers AST-1138766 and AST-1536171. The DES participants from Spanish institutions are partially supported by MINECO under grants AYA2015-71825, ESP2015-66861, FPA2015-68048, SEV-2016-0588, SEV-2016-0597, and MDM-2015-0509, some of which include ERDF funds from the European Union. IFAE is partially funded by the CERCA program of the Generalitat de Catalunya. Research leading to these results has received funding from the European Research Council under the European Union’s Seventh Framework Program (FP7/2007-2013) including ERC grant agreements 240672, 291329, and 306478. We acknowledge support from the Australian Research Council Centre of Excellence for All-sky Astrophysics (CAASTRO), through project number CE110001020.

This manuscript has been authored by Fermi Research Alliance, LLC under Contract No. DE-AC02-07CH11359 with the U.S. Department of Energy, Office of Science, Office of High Energy Physics. The United States Government retains and the publisher, by accepting the article for publication, acknowledges that the United States Government retains a non-exclusive, paid-up, irrevocable, world-wide license to publish or reproduce the published form of this manuscript, or allow others to do so, for United States Government purposes.

This paper has gone through internal review by the DES collaboration. The DES publication number for this article is DES-2017-0307.

REFERENCES

Abbott T. M. C., et al., 2017b, preprint, (arXiv:1708.01530)
Abbott T. M. C., et al., 2017a, Submitted to: Mon. Not. Roy. Astron. Soc.
Alam S., et al., 2017, Mon. Not. Roy. Astron. Soc., 470, 2617
Anderson L., et al., 2014a, Mon. Not. Roy. Astron. Soc., 439, 83
Anderson L., et al., 2014b, MNRAS, 441, 24
Ata M., et al., 2018, Mon. Not. Roy. Astron. Soc., 473, 4773
Avila S., Murray S. G., Knebe A., Power C., Robotham A. S. G., Garcia-Bellido J., 2015, Mon. Not. Roy. Astron. Soc., 450, 1856
Avila S., et al., 2017, Submitted to: Mon. Not. Roy. Astron. Soc.
Blake C., Collister A., Bridle S., Lahav O., 2007, Mon. Not. Roy. Astron. Soc., 374, 1527
Blake C., et al., 2011, Mon. Not. Roy. Astron. Soc., 418, 1707
Brown M. L., Castro P. G., Taylor A. N., 2005, Mon. Not. Roy. Astron. Soc., 360, 1262
Carnero A., Sanchez E., Crocce M., Cabre A., Gaztanaga E., 2012, Mon. Not. Roy. Astron. Soc., 419, 1689
Cawthon R., et al., 2017, Submitted to: Mon. Not. Roy. Astron. Soc.
Chan K. C., et al., 2018, preprint, (arXiv:1801.04390)
Coe S., et al., 2005, Mon. Not. Roy. Astron. Soc., 362, 505
Cowan G., 1998, Statistical data analysis. Oxford University Press, UK
Crocce M., Fosalba P., Castander F. J., Gaztaña E., 2010, MNRAS, 403, 1553
Crocce M., Cabré A., Gaztaña E., 2011, MNRAS, 414, 329
Crocce M., Castander F. J., Gaztaña E., Fosalba P., Carretero J., 2015, Mon. Not. Roy. Astron. Soc., 453, 1513
Crocce M., et al., 2016, MNRAS, 455, 4301
Crocce M., et al., 2017, Submitted to: Mon. Not. Roy. Astron. Soc.
Davis C., et al., 2017, Submitted to: Mon. Not. Roy. Astron. Soc.
De Vicente J., Sánchez E., Sevilla-Noarbe I., 2016, Mon. Not. Roy. Astron. Soc., 459, 3078
Dodelson S., 2003, Modern Cosmology. Academic Press, Amsterdam, http://www.slac.stanford.edu/spires/find/books/www?c1=Q8961:D62:2003
Dodelson S., Schneider M. D., 2013, Phys. Rev. D, 88, 063537
Dvlca-Wagner A., et al., 2018, ApJS, 235, 33
Efstathiou G., 2004, Mon. Not. Roy. Astron. Soc., 349, 603
Eisenstein D. J., Hu W., 1998, Astrophys. J., 496, 605
Eisenstein D. J., Zehavi I., Hogg D. W., Scoccimarro R., Blanton M. R., Nichol R. C., Scranton R. e. a., 2005, ApJ, 633, 560
Flaugher B., 2005, Int. J. Mod. Phys., A20, 3121
Flaugher B., et al., 2015, AJ, 150, 150
Foreman-Mackey D., Hogg D. W., Lang D., Goodman J., 2013, PASP, 125, 306
Fosalba P., Gaztaña E., Castander F. J., Croce M., 2015a, Mon. Not. Roy. Astron. Soc., 447, 1319
Fosalba P., Croce M., Gaztaña E., Castander F. J., 2015b, Mon. Not. Roy. Astron. Soc., 448, 2987
Gatti M., et al., 2017, Submitted to: Mon. Not. Roy. Astron. Soc.
Gil-Marín H., de Vicente J., Sánchez E., Sevilla-Noarbe I., 2016, Mon. Not. Roy. Astron. Soc., 459, 3078
Gruen D., et al., 2018, Phys. Rev. D, 98, 023507
Hartlap J., Simon P., Schneider P., 2007, A&A, 464, 399
Hivon E., Gorski K. M., Netterfield C. B., Wandelt B. D., Hansen F. K., Reinecke M., Bartelman M., 2005, Astrophys. J., 622, 759
Gruen D., et al., 2018, Phys. Rev. D, 98, 023507
Hoyle B., 2012, MNRAS, 421, 1527
Hoyle B., 2018, MNRAS, 478, 592
Krause E., et al., 2017, Submitted to: Phys. Rev. D
Limber D. N., 1953, AJ, 117, 134
Lyth D. H., Liddle A. R., 2009, The primordial density perturbation: Cosmology, inflation and the origin of structure. Cambridge University Press, UK, http://www.cambridge.org/uk/catalogue/catalogue.asp?isbn=9780521828499
Padmanabhan N., Xu X., Eisenstein D. J., Scalzo R., Cuesta A. J., Mehta K. T., Kazin E., 2012, Mon. Not. Roy. Astron. Soc., 427, 2132
Percival W. J., et al., 2001, Mon. Not. Roy. Astron. Soc., 327, 1297
Percival W. J., et al., 2014, MNRAS, 439, 2531
Ross A. J., Samushia L., Howlett C., Percival W. J., Burden A., Manera M., 2015, Mon. Not. Roy. Astron. Soc., 449, 835
Ross A. J., et al., 2017, Mon. Not. Roy. Astron. Soc.
Sawangwit U., Shanks T., Abdalla F. B., Cannon R. D., Croom S. M., Edge A. C., Ross N. P., Wake D. A., 2011, MNRAS, 416, 3033
Seo H.-J., et al., 2012, Astrophys. J., 761, 13
Sobreira F., de Simoni F., Rosenfeld R., da Costa L. A. N., Maia M. A. G., Makler M., 2011, Phys. Rev., D84, 103001
de Simoni F., et al., 2013, Mon. Not. Roy. Astron. Soc., 435, 3017
AFFILIATIONS

1 Departamento de Física Matemática, Instituto de Física, Universidade de São Paulo, CP 66318, São Paulo, SP, 05314-970, Brazil
2 Laboratório Interinstitucional de e-Astronomia - LineA, Rua Gal. José Cristino 77, Rio de Janeiro, RJ - 20921-400, Brazil
3 Instituto de Física Teórica, Universidade Estadual Paulista, São Paulo, Brazil
4 ICTP South American Institute for Fundamental Research, P. O. Box 586, Trieste, Italy
5 Departament de Física Teòrica and Center for Astroparticle Physics, Universitat de Genève, Quai Ernest Ansermet, CH-1211 Geneva, Switzerland
6 Instituto de Física Gleb Wataghin, Universidade Estadual de Campinas, 13083-859, Campinas, SP, Brazil
7 Observatório Nacional, Rua Gal. José Cristino 77, Rio de Janeiro, RJ - 20921-400, Brazil
8 Institute of Cosmology & Gravitation, University of Portsmouth, Portsmouth, PO1 3FX, UK
9 Institut d’Estudis Espacials de Catalunya (IEEC), 08193 Barcelona, Spain
10 Institute of Space Sciences (ICE, CSIC), Campus UAB, Carrer de Can Magrans, s/n, 08193 Barcelona, Spain
11 Center for Cosmology and Astro-Particle Physics, The Ohio State University, Columbus, OH 43210, USA
12 Instituto de Física Teorica UAM/CSIC, Universidad Autónoma de Madrid, 28049 Madrid, Spain
13 Cerro Tololo Inter-American Observatory, National Optical Astronomy Observatory, Casilla 603, La Serena, Chile
14 Department of Physics & Astronomy, University College London, Gower Street, London, WC1E 6BT, UK
15 Department of Physics and Electronics, Rhodes University, PO Box 94, Grahamstown, 6140, South Africa
16 Fermi National Accelerator Laboratory, P. O. Box 500, Batavia, IL 60510, USA
17 Observatories of the Carnegie Institution of Washington, 813 Santa Barbara St., Pasadena, CA 91101, USA
18 CNRS, UMR 7095, Institut d’Astrophysique de Paris, F-75014, Paris, France
19 Sorbonne Universités, UPMC Univ Paris 06, UMR 7095, Institut d’Astrophysique de Paris, F-75014, Paris, France
20 Jodrell Bank Center for Astrophysics, School of Physics and Astronomy, University of Manchester, Oxford Road, Manchester, M13 9PL, UK
21 Kavli Institute for Particle Astrophysics & Cosmology, P. O. Box 2450, Stanford University, Stanford, CA 94309, USA
22 SLAC National Accelerator Laboratory, Menlo Park, CA 94025, USA
23 Department of Astronomy, University of Illinois at Urbana-Champaign, 1002 W. Green Street, Urbana, IL 61801, USA
24 National Center for Supercomputing Applications, 1205 West Clark St., Urbana, IL 61801, USA
25 Institut de Física d’Altes Energies (IFAE), The Barcelona Institute of Science and Technology, Campus UAB, 08193 Bellaterra (Barcelona) Spain
26 Kavli Institute for Cosmological Physics, University of Chicago, Chicago, IL 60637, USA
27 Department of Physics and Astronomy, University of Pennsylvania, Philadelphia, PA 19104, USA
28 Centro de Investigaciones Energéticas, Medioambientales y Tecnológicas (CIEMAT), Madrid, Spain
29 Department of Physics, IIT Hyderabad, Kandi, Telangana 502285, India
30 Department of Astronomy, University of Michigan, Ann Arbor, MI 48109, USA
31 Department of Physics, University of Michigan, Ann Arbor, MI 48109, USA
32 Institute of Astronomy, University of Cambridge, Madingley Road, Cambridge CB3 0HA, UK
33 Kavli Institute for Cosmology, University of Cambridge, Madingley Road, Cambridge CB3 0HA, UK
34 Universität-Sternwarte, Fakultät für Physik, Ludwig-Maximilians Universität München, Scheinerstr. 1, 81679 München, Germany
35 Santa Cruz Institute for Particle Physics, Santa Cruz, CA 95064, USA
36 Department of Physics, The Ohio State University, Columbus, OH 43210, USA
37 Max Planck Institute for Extraterrestrial Physics, Giessenbachstrasse, 85748 Garching, Germany
38 Harvard-Smithsonian Center for Astrophysics, Cambridge, MA 02138, USA
39 Department of Astronomy/Steward Observatory, 933 North Cherry Avenue, Tucson, AZ 85721-0065, USA
40 Jet Propulsion Laboratory, California Institute of Technology, 4800 Oak Grove Dr., Pasadena, CA 91109, USA
41 Australian Astronomical Observatory, North Ryde, NSW 2113, Australia
42 George P. and Cynthia Woods Mitchell Institute for Fundamental Physics and Astronomy, and Department of Physics and Astronomy, Texas A&M University, College Station, TX 77843, USA
43 Institución Catalana de Recerca i Estudis Avançats, E-08010 Barcelona, Spain
44 Department of Physics and Astronomy, University of Waterloo, 200 University Ave W, Waterloo, ON N2L 3G1, Canada
45 Perimeter Institute for Theoretical Physics, 31 Caroline St. North, Waterloo, ON N2L 2Y5, Canada
46 Department of Physics and Astronomy, Pevensey Building, University of Sussex, Brighton, BN1 9QH, UK
47 School of Physics and Astronomy, University of Southampton, Southampton, SO17 1BJ, UK
48 Brandeis University, Physics Department, 415 South Street, Waltham MA 02453
49 Computer Science and Mathematics Division, Oak Ridge National Laboratory, Oak Ridge, TN 37831
50 Institute for Astronomy, University of Edinburgh, Edinburgh EH9 3HJ, UK

This paper has been typeset from a TeX/LaTeX file prepared by the author.