The mechanism of the collapse of the superhydrophobic state is elucidated for submerged nanoscale textures forming a three-dimensional interconnected vapor domain. This key issue for the design of nanotextures poses significant simulation challenges as it is characterized by diverse time and length scales. State-of-the-art atomistic rare events simulations are applied for overcoming the long time scales connected with the large free energy barriers. In such interconnected surface cavities wetting starts with the formation of a liquid finger between two pillars. This break of symmetry induces a more gentle bend in the rest of the liquid-vapor interface, which triggers the wetting of the neighboring pillars. This collective mechanism, involving the wetting of several pillars at the same time, could not be captured by previous atomistic simulations using surface models comprising a small number of pillars (often just one). Atomistic results are interpreted in terms of a sharp-interface continuum model which suggests that line tension, condensation, and other nanoscale phenomena play a minor role in the simulated conditions.

DOI: 10.1103/PhysRevFluids.2.034202

I. INTRODUCTION

Superhydrophobicity stems from the presence of a gaseous layer between a body of liquid and a surface. This suspended “Cassie” state is fostered by surface roughness and hydrophobic coatings [1]; the composite liquid-gas-solid interface results in important properties for submerged and “dry” technological applications, such as self-cleaning, enhanced liquid repellency, and drag reduction [2,3]. The superhydrophobic Cassie state is sustained by capillary forces, which can be overcome by variations in the liquid pressure, temperature, or other external forces which trigger the transition to the fully wet Wenzel state. Thus, the design of textured surfaces and coatings has the aim of realizing a robust Cassie state.

The stability of the Cassie state depends not only on the thermodynamic conditions but also on the surface geometry and chemistry, which can be engineered in order to achieve robust superhydrophobicity. Hydrophobic textures of nanometric size [4,5] proved efficient in stabilizing the gaseous layer over a broad range of pressures and temperatures [6]. However, the engineering of surface nanotextures is still in its infancy: understanding the collapse mechanism, i.e., the path followed by the liquid front during the breakdown of the Cassie state, is the key to improving the performance and robustness of such textures. For instance, it is possible to modify surfaces in order to destabilize the Wenzel state [7] or to achieve robust superhydrophobicity via complex nanotextures [8]. Nucleation of gas and vapor bubbles, which is enhanced by surface textures [9], can also bring about the breakdown of the Cassie state; superhydrophobic surfaces must be engineered to prevent it. However, to date the collapse mechanism on experimentally and technologically relevant textures remains largely unknown, with the theoretical approaches making a priori assumptions or often being affected by simulation artifacts as discussed in detail below.
Due to their simplicity, surfaces decorated with pillars are a paradigm in the study of superhydrophobicity, both via experiments and simulations. In addition, because of the reduced liquid-solid contact, these kind of textures favor the emergence of large slip at the walls [10], making them attractive, e.g., for drag reduction [3]. The focus of this work is the wetting of three-dimensional (3D) submerged nanopillars (Fig. 1): the three distinctive attributes of the textures studied in this work are submerged, 3D, and nanoscale. Indeed, most simulations to date have restricted their attention to drops of sizes comparable to that of the texture at the top of which they are sitting [11–17]; in this setup the collapse mechanism is significantly influenced by the drop shape and size. At variance with drops, the main issue for submerged surfaces is the resistance of the superhydrophobic state against pressure variations [7,8,18–21]. Present superhydrophobic surfaces generally exhibit complex 3D morphologies with isolated (pores) or connected (pillars, cones) cavities. Two-dimensional (2D) or quasi-2D (limited thickness) models have been often used in simulations with the aim of reducing their computational cost [8,14,17–19]. However, systems such as pillarred surfaces cannot be reduced to 2D without overlooking important phenomena, e.g., the simultaneous wetting of several interpillar spacings. Concerning the methods, mainly due to the significant computational cost, most approaches dealing with 3D structures to date considered a continuum description of the liquid (and solid) [15–17,22–24], which necessarily introduces some assumptions concerning the structure of the interfaces, the interaction with the wall, and other nanoscale effects such as fluctuations, line tension, etc. Such effects are in principle relevant at the nanoscale. In order to avoid these limitations and explore the fundamentals of wetting of experimentally relevant, 3D nanotextures, here the collapse mechanism of a large sample containing a three-by-three array of pillars is identified via molecular dynamics (MD) combined with the string method in collective variables. Other atomistic approaches have been recently employed which, however, lead to a discontinuous dynamics for the collapse of the meniscus [7] (a detailed analysis of this problem is reported elsewhere [25]).

In brief, the objective of this work is addressing two open questions: (1) finding the most probable collapse mechanism for submerged nanopillars and computing the associated free energy profile; and (2) validating simple continuum models for nanoscale wetting, identifying which bulk, interface, and line terms are relevant.
COLLAPSE OF SUPERHYDROPHOBICITY ON . . .

Two challenges are inherent to these problems: (1) employ a model which captures the physics at the nanoscale, including fluctuations, evaporation and condensation, and line tension; and (2) interpret the results in simple terms, which can be used for developing design criteria. In this work, a Lennard-Jones (LJ) fluid and solid are used to tackle the first challenge. This approach is computationally expensive but includes all the relevant physics with minimal assumptions [26]. Concerning the second, a sharp-interface continuum model is used to interpret the atomistic results, which yields a simple and informative picture of the phenomena and allows us to shed light on the nanoscale effects. Results show that, differently from previous studies focusing on independent cavities [25,27], the collapse mechanism for pillars is characterized by the combination of local and collective effects. In particular, the meniscus breaks the symmetry imposed by the confining geometry and the collapse happens via the local formation of a single liquid finger followed by the correlated, collective wetting of the interpillar space of points far apart on the surface.

In interconnected geometries the meniscus is expected to assume complex morphologies during the collapse. In the present study the (atomistic) density field $\rho(x)$ is used in order to monitor the process: this choice allows one to track any changes in the meniscus shape and, at the same time, is straightforward to compute in atomistic simulations (Fig. 1). The most probable wetting path is identified via the string method by using the density field to characterize the system configuration. The identified path corresponds to a sequence of density fields $\rho(x)$ at discrete steps along the collapse process. The string method also allows for computing the free energy along the most probable path $\Omega[\rho(x)]$ and, thus, the free energy barrier determining the kinetics of the process. Indeed, we show that, even at relatively large liquid pressures, wetting requires that the system climbs a sizable free energy barrier, which is possible only because of thermal fluctuations [28,29].

The paper is organized in a methodological section (Sec. II), in which the main conceptual aspects of the string method are described, and a second, self-contained section in which the results on the collapse of the superhydrophobic state are discussed in depth. Thus, the reader interested only in the physical results can go directly to this Sec. III. The final section is left for conclusions.

II. METHODS

Typically, large free energy barriers separate the Cassie and Wenzel states. This means that, even if thermodynamics might favor the process, i.e., the final is state more stable than the initial one, the system still has to climb the free energy up to a saddle point (barrier) for the wetting transition to take place. This is different from barrierless processes; in the presence of a barrier wetting is possible only because of thermal fluctuations, which determine the time scale for observing a transition event. This time scale is too long to be accessed by brute force MD: this is the problem of rare events [28]. To cope with this issue, here the string method in collective variables (CVs) is used [30]. This method allows one to follow the infrequent process at fixed thermodynamics conditions (i.e., without increasing pressure and temperature), which implies visiting configurations characterized by high free energies and a corresponding, exponentially low probability.

CVs at the basis of the string method are a (restricted) set of observables $\{\theta_i(r)\}_{i=1,M}$ function of $r$, the $3n_f$-dimensional vector of the fluid particles positions. CVs should correspond to the degrees of freedom which are able to characterize the system along the transition from the initial to the final state. Here we employ the coarse-grained density field, which has been used in recent works on wetting transitions [18,25] and other hydrophobicity-related phenomena [31]. Moreover, the density field is the cornerstone of most of meso- and macroscopic descriptions of homogeneous and heterogeneous fluids, e.g., the classical Density Functional Theory [32,33]. Thus, the coarse-grained density is a natural CV to study the collapse of the Cassie state.

The coarse-grained density field is defined as

$$\theta_i(r) \equiv \theta(r,x_i) = \frac{1}{\Delta V} \sum_{j=1}^{n_f} \tilde{\chi}(r_j,x_i),$$

(1)
where $\theta(r,x_i)$ is the density at the point $x_i$ of the discretized (or coarse-grained) ordinary space [Fig. 1(b)] and $\tilde{\chi}(r_j,x_i)$ is a smoothed approximation to the characteristic function of the volume $\Delta V$ around the point $x_i$, with the sum at the right-hand side (RHS) running over the $n_f$ fluid particles. In practice, these functions count the number of atoms in each cell in Fig. 1(b). In the following, whenever possible, $\theta_i(r) = \theta(r,x_i)$ is replaced by the lighter notation $\theta(r,x)$, which denotes the CV at all points $x_i$ of the discretized space, and $\rho(x)$ a realization of this CV. Although $\theta(r,x)$, and analogously $\rho(x)$, is interpreted as a coarse-grained density field, we find it sometimes convenient to consider it as an $M$-dimensional vector with components $\theta_i(r)$ ($\rho_i$, respectively).

Our aim is to find and characterize the most probable path $\rho(x;\tau)$ followed by the system along the Cassie-Wenzel transition. This path represents a curve in the space of the coarse-grained density or, more visually, a series of snapshots taken at successive times $\tau$ along the wetting process. The parametrization of this curve with the time $\tau$ of the transition is unpractical in actual calculations [34]. A more convenient but equivalent parametrization is the normalized arc-length parametrization, i.e., the parametrization according to the length of the curve $\rho(x;\tau)$ at a given time $\tau$, divided by the total length of the curve: $\lambda = \int_{\rho_c}^{\rho_w} d\rho/\int_{\rho_c}^{\rho_w} d\rho$, where $\rho_c$ and $\rho_w$ are the density fields corresponding to the Cassie and Wenzel states, respectively, and $d\rho = \sqrt{\sum_{i=1,M} \left[\partial \rho(x_i,\tau)/\partial \tau \right]^2} d\tau$.

An infinite number of paths exists that bring the system from the Cassie to the Wenzel state. The objective of the string method is to find the most probable one, which, under the assumptions explained in the Appendix, must satisfy the condition [30]

$$\{g[\rho(x;\lambda)]\nabla_\rho \Omega[\rho(x;\lambda)] \}_{\perp} = 0,$$

(2)

where $\nabla_\rho$ is the vector of derivatives with respect to the different components of the collective variable $\rho$, namely, the vector whose components are $\partial/\partial \rho_i$ with $i = 1, \ldots, M$. Here the symbol $\perp$ denotes “orthogonal to the path $\rho(x;\lambda)$”; $\Omega[\rho(x;\lambda)]$ is the Landau free energy of the coarse-grained density field $\rho(x;\lambda)$ along the string. This free energy is in general related to the probability of observing the realization $\rho(x)$ of the coarse-grained density under the atomistic probability distribution $m(r)$:

$$\begin{aligned}
\Omega[\rho(x)] & = -k_B T \ln p(\rho(x)) = -k_B T \ln \left\{ \int \text{d}r \ m(r) \prod_{i=1}^{M} \delta[\theta(r,x_i) - \rho(x_i)] \right\}.
\end{aligned}$$

(3)

The $i$-$j$ components of the metric tensor $\hat{g}[\rho(x)]$ in Eq. (2) read

$$g_{ij}[\rho(x)] = \frac{\int \text{d}r \ \nabla_\rho \theta(r,x_i) \cdot \nabla_\rho \theta(r,x_j) \ m(r) \prod_{l=1}^{M} \delta[\theta(r,x_l) - \rho(x_l)]}{\int \text{d}r \ m(r) \prod_{l=1}^{M} \delta[\theta(r,x_l) - \rho(x_l)]},$$

(4)

where $\nabla_\rho$ denotes the $3n_f$-dimensional vector of the derivatives with respect to the components of the particle positions, $\partial/\partial r_\alpha$, with $\alpha = 1, \ldots, n_f$ and $l = x, y, z$.

The intuitive meaning of Eq. (2) is that the component of the force $\hat{g}(\rho(x;\lambda))\nabla_\rho \Omega[\rho(x;\lambda)]$ orthogonal to the path is zero. To give a visual interpretation, $\Omega[\rho(x)]$ should be imagined as a rough free energy landscape; a path satisfying condition (2) lies at the bottom of a valley connecting the initial and final states (free energy minima) and passes through a mountain pass (free energy saddle point).

In atomistic simulations, $\hat{g}(\rho(x;\lambda))$ and $\nabla_\rho \Omega[\rho(x;\lambda)]$ can be estimated, for each point $\lambda$ constituting the string, by an MD governed by the following equations of motion [35]:

$$m_a \ddot{r}_a = -\nabla_{r_a} V(r) - k \sum_{i=1}^{M} \left[ \theta(r,x_i) - \rho(x_i;\lambda) \right] \nabla_{r_a} \theta(r,x_i) + \text{thermo}(T) + \text{baro}(P),$$

(5)

where $m_a$ is the mass of the $\alpha$th particle, $\alpha = 1, \ldots, n_f$, $V(r)$ is the interparticle potential, and $k \sum_{i=1}^{M} \left[ \theta(r,x_i) - \rho(x_i;\lambda) \right] \nabla_{r_a} \theta(r,x_i)$ is a biasing force which allows the system to visit regions of the phase space around the condition $\theta(r,x) = \rho(x;\lambda)$. The biasing force makes it possible to estimate the gradient of the free energy and the metric matrix of points having a very low probability
(high free energy), such those near the transition state. In practice, \(\hat{\omega}[\rho(x; \lambda)]\) and \(\nabla_{\rho}\Omega[\rho(x; \lambda)]\) are computed as time averages along the MD of Eq. (5):

\[
g_{ij}[\rho(x; \lambda)] = \frac{1}{t_{MD}} \int_{0}^{t_{MD}} ds \ \nabla_{\rho} \theta[r(s), x_{i}] \cdot \nabla_{\rho} \theta[r(s), x_{j}],
\]

\[
\frac{\partial \Omega[\rho(x; \lambda)]}{\partial \rho_{i}} = - \frac{1}{t_{MD}} \int_{0}^{t_{MD}} ds \ \{\theta[r(s), x_{i}] - \rho(x_{j}; \lambda)\},
\]

with \(t_{MD}\) the duration of the MD simulation and the indices \(i\) and \(j\) running over the \(M\) coarse-graining cells.

The (improved) string method [34] is an iterative algorithm that, starting from a first-guess path, produces the most probable path \(\rho(x; \lambda)\) satisfying Eq. (2). Here we refrain from describing the algorithm in detail, summarizing only the main steps of the method. For further details the interested reader is referred to the Appendix, to the original article [34], or to reviews [28]. In the string method, the continuum path \(\rho(x; \lambda)\), with \(0 \leq \lambda \leq 1\), is replaced by its discrete counterpart \(\{\rho(x; \lambda_{n})\}_{n=1,L}\), with \(L\) the number of snapshots used to discretize the path. The algorithm starts from a first guess of the wetting path, \(\{\rho_{0}(x; \lambda_{n})\}_{n=1,L}\), and performs an iterative minimization procedure, which yields a path with zero orthogonal component of the force: \(\langle \{\hat{\omega}[\rho(x; \lambda_{n})] \nabla_{\rho} \Omega[\rho(x; \lambda_{n})] \rangle_{s} = 0 \rangle_{n=1,L}\). At each iteration, \(\{\hat{\omega}[\rho(x; \lambda_{n})]\}_{n=1,L}\) and \(\{\nabla_{\rho} \Omega[\rho(x; \lambda_{n})]\}_{n=1,L}\) are computed by the biased MD in Eq. (5) and are used to generate a new path. The procedure is performed until convergence is reached, i.e., when the difference in the free energy of each image between two string iterations is below a prescribed threshold (see the Supplemental Material for convergence plots [36]).

Along the path of maximum probability one can compute the free energy profile and the associated barrier \(\Omega_{1}\), which can in turn be related to the wetting and (dewetting) transition time \(t_{CW}(t_{WC})\) via the transition state theory: \(t_{CW} = t_{0}^{0} \exp[\Omega_{CW}^{i}/k_{B} T]\) \(t_{WC} = t_{0}^{0} \exp[\Omega_{WC}^{i}/k_{B} T]\). In the present article, the free energy profile along the most probable wetting path is reported against the filling fraction \(\Phi(\lambda_{n}) = \{N(\lambda_{n}) - N_{C}\}/\{N_{W} - N_{C}\}\), where \(N(\lambda_{n}) \equiv \Delta V \sum_{i}^{M} \rho(x_{i}; \lambda_{n})\) is the number of liquid particles in the yellow region of Fig. 1(b) at the string point \(\lambda_{n}\) and \(N_{C}\) and \(N_{W}\) are the number of particles in the Cassie and Wenzel states, respectively. In the present calculations, \(N\) and \(\Phi\) are nondecreasing functions of \(\lambda\) along the wetting path; thus, the filling fraction can be used as an \textit{a posteriori} parametrization of the most probable wetting path \(\rho(x; \Phi)\). It is important to remark that this does not imply that \(\Phi\) is a good CV for the wetting transition in interconnected textured surfaces of the type studied in this article. In fact, as shortly discussed in the next section, and more extensively in a forthcoming article, using \(\Phi\) or \(\theta\) as CVs leads to qualitatively different results, with those of the first CV characterized by an unphysically discontinuous path.

Summarizing, the aim of the string method in CVs is to compute the most probable path in a complex high-dimensional free energy landscape. This is different from the objective and approach of other techniques (e.g., umbrella sampling, restrained MD, boxed MD, etc.), which entail reconstructing the entire landscape within a predefined volume of the CV space. The advantage of the string method is that it scales linearly with the number of CVs, while more standard methods scale exponentially. This allowed us to investigate the collapse mechanism in the high-dimensional space (864 degrees of freedom) of the coarse-grained density field, which would have been impossible with other approaches.

MD simulations for computing \(\{\hat{\omega}[\rho(x; \lambda_{n})]\}_{n=1,L}\) and \(\{\nabla_{\rho} \Omega[\rho(x; \lambda_{n})]\}_{n=1,L}\) are performed at constant pressure, temperature, and number of particles [36]. The LJ fluid is characterized by a potential well of depth \(\varepsilon\) and a length scale \(\sigma\). The (modified) attractive term of the LJ potential between the fluid and solid particles is scaled by a constant to yield a Young contact angle on a flat surface \(\theta_{Y} = 113^\circ\). The pressure is close to the liquid-vapor bulk coexistence, \(\Delta P \equiv P_{L} - P_{v} \approx 0\), while the temperature is \(T = 0.8 \ v_{s}^{-1}\). Free energy profiles at different pressures can be obtained by simply adding an analytical bulk term of the form \(\langle P_{L} - P_{v} \rangle V_{v}\), with \(V_{v}\) the volume of the vapor bubble [7,20,24,38,39], which can be obtained from the number of fluid particles in the cavity region (the yellow framework in Fig. 1). The first guess for the string calculation is obtained by
running an MD simulation at high pressure. In this condition the wetting barrier is small enough that the transition occurs on the time scale accessible by brute-force MD. We remark that the rest of simulations for the iterative string calculations are not run at such high pressure but close to coexistence, as said above. The simulations are run via a modified version of the LAMMPS software [40].

III. RESULTS AND DISCUSSION

A. Mechanism of collapse

The Cassie-Wenzel transition can take place following different wetting paths; here we analyze the one having the highest probability. At the pressures and temperatures of interest for technological applications (e.g., drag reduction), the Cassie and Wenzel states are separated by large free energy barriers that the system has to overcome. Thus, even if thermodynamics might favor the collapse, the system still has to climb the free energy barrier separating the initial and final state. This apparently nonspontaneous process can take place only because of thermal fluctuations [28,29]. This implies infrequent transition events or, which is equivalent, long transition times, much longer than the typical time scale accessible to brute force (standard) MD. Thus, here the most probable wetting path is computed using a special technique: the string method in collective variables [30], which is described in detail in Sec. II. It is important to remark that in the string method the pressure and temperature are kept constant at the prescribed values; in other words, the path obtained via the string method is representative of the transition at constant pressure and temperature.

The path is constituted by a sequence of atomistic coarse-grained density fields \( \rho(x) \) [Eq. (1)]; i.e., the path can be seen as a series of snapshots of the density field taken at different times along the transition from the Cassie to the Wenzel state. It is important to remark that each \( \rho(x) \) is obtained by performing the ensemble average over atomistic configurations consistent with the state of the system along the path; thus, \( \rho(x) \) contains all the nanoscale information. The morphology of the interface between the liquid and the vapor domains, the meniscus, is a simpler and more visual observable to follow the collapse mechanism. Thus, in the following the meniscus, which can be computed from \( \rho(x) \), will be used to describe the change of morphologies of the liquid along the collapse process, and its effect on the free energy. These morphologies will be discussed in detail, with particular attention to clarify the role of nanoscale aspects such as line tension.

Figure 2 shows the collapse mechanism of the superhydrophobic state and the related free energy profile \( \Omega(\Phi) \) along the most probable wetting path at a pressure and temperature close to the Cassie-Wenzel coexistence (i.e., where the Cassie and Wenzel states have approximately the same free energy, \( T = 0.8 \varepsilon k_B^{-1} \) and \( \Delta P = 0.011 \varepsilon \sigma^{-3} \)). \( \Phi \) denotes the filling fraction defined as \( \Phi \equiv (N - N_C)/(N_W - N_C) \), with \( N \) the total number of liquid particles in the yellow regions of Fig. 1(b) and \( N_C \) and \( N_W \) the number of particles in the Cassie and Wenzel states, respectively. Here and in the following, notations of the type \( \Omega(\Phi) \) are used as a shorthand for the more complete notation \( \Omega(\rho(x; \Phi)) \). The wetting path is divided into five parts (I–V), corresponding to different regimes.

In I, the meniscus is pinned at the top corners of the pillars, with its curvature increasing with \( \Phi \). The free energy minimum corresponds to the Cassie state, which is characterized by an almost flat meniscus.

In II, the meniscus depins from the corners and progressively slides along the pillars filling the interpillar space. The liquid-vapor interface has a small curvature which is sufficient to meet the pillars with the Young contact angle. Configurations in II correspond to a linear increase of the free energy. Given the large ratio between the height of the pillars and the spacing among them, the “sag” mechanism [27,41], in which the meniscus remains pinned at the pillars corner along the entire process, cannot be realized.

The transition state (TS, free energy maximum) is found in III and corresponds to the liquid touching the bottom wall. In this part of the transition, the shape of the liquid-vapor interface
changes dramatically: starting from an almost flat interface a liquid finger forms between two pillars and then touches the bottom wall [see Fig. 2(a) and Ref. [42]]. The free energy barrier for collapse is very high for the considered pressure $\Delta P = 0.011 \varepsilon \sigma^{-3}$, $\Delta \Omega_{C_W} = 670 k_B T$. From this contact point, the liquid progressively fills the surrounding interpillar spaces. In the regions in which the liquid touches the bottom, the double liquid-vapor–vapor-solid interface is replaced by the liquid-solid interface, causing the free energy to decrease. It is clear that identifying correctly the most probable TS is especially important because this configuration determines the free energy barrier and, with exponential sensitivity, the collapse kinetics. In Sec. III C comparison with other mechanisms proposed in the literature [7,41] shows how seemingly small morphological changes are reflected in radically different estimates of these quantities.

A closer look to the configurations around the TS shows that the finger formation involves both quasi-2D and collective wetting of the pillars (Fig. 3). In one direction (green line in Fig. 3), the liquid finger is strongly confined between pillars. Confinement renders the wetting mechanism effectively 2D close to the pillars centers, as demonstrated by comparing the second cut of the...
FIG. 3. Two-dimensional cuts of the number density at the transition state: the liquid finger (identified by the hand symbol) forms at the intersection of the red and green planes. Bulk liquid density is represented in blue and vapor in white; black isolines identify the liquid-vapor interface. The density field at the top right is taken from the string simulations of Ref. [25], where a quasi-2D groove is considered.

Density field in Fig. 3 with the 2D mechanisms of previous works [25]: the wetting of the bottom wall happens via the formation of two asymmetric bubbles at the pillars lower corners with the smaller bubble disappearing faster. In the orthogonal direction (red line in Fig. 3) and far from the confined finger (blue line) the liquid-vapor interface must bend in order to recover the flat shape; the ensuing curvature of the interface is gentle because of surface tension. This collective, large-scale mechanism triggers the wetting of the interpillar spaces surrounding the initial finger, causing the final collapse of the vapor domain.

Figures 2(a) and 3 show that the collapse is asymmetric and involves many interpillars spacings; this fact suggests that assuming a symmetric mechanism [41] or simulating a single elementary cell is insufficient to capture correctly the mechanism and the related free energy since it imposes an unphysical symmetry to the problem. Even for the large domain simulated here, the effect of periodic boundary conditions becomes apparent at large filling levels beyond the TS; this, however, does not affect the estimation of the free energy barriers.

The present simulations can also help understanding the mechanism of the opposite process, i.e., the dewetting transition from Wenzel to Cassie. Indeed, under the hypothesis of a quasistatic transformation implicit in the string method, the forward and backward processes happen reversibly along the same path [43]. Thus, here we describe the Wenzel-Cassie process associated to the path in Fig. 2 paying particular attention to the aspects relevant to dewetting. In order to do that, in Fig. 4 we report the free energy profile at conditions close to bulk liquid vapor coexistence, \( \Delta P \approx 0 \). Dewetting, which corresponds to the nucleation of a vapor domain in the textured surface, starts with the formation of two low-density, flat domains at the bottom of two facing pillars. These domains grow and merge, forming a single depleted region between the pillars. This region then percolates to the neighboring pillars, forming a connected network. While the string identifies only one percolating network, the texture geometry suggests that many such networks are possible, all of which involve multiple pillars. It must be stressed that this initial “collective” nucleation process, which corresponds to part V of Fig. 2, cannot be captured by simulating a single pillar or an elementary cell in one or two directions [7,14,19,24]. Further moving toward the Cassie state, the percolating, depleted domain starts to form also in the spaces among four pillars and detaches from the bottom forming a proper bubble. This part of the path corresponds to domain IV, where the
free energy shows a descending trend with different slope. This branch of the process is completed when the liquid finger finally detaches from the bottom of the surface in a point between two pillars, domain III. The free energy barrier for dewetting at $\Delta P \approx 0$ is $480 \, k_BT$.

**B. A sharp-interface interpretation of the atomistic mechanism**

In order to rationalize the atomistic results in simple energetic terms, a macroscopic, sharp-interface model of capillarity is used in connection with the data summarized in Fig. 2. For this model the (excess) free energy reads [44]

$$\Omega_{\text{macro}} = \Omega - \Omega_{\text{ref}} = \Delta P V_v + \gamma_{lv}(A_{lv} + \cos \theta_Y A_{sv}),$$

where the Wenzel free energy $\Omega_{\text{ref}} = P_l V_{tot} + \gamma_{sl} A_{tot}$ is taken as a reference and $V_{tot}$ and $A_{tot}$ are the total volume of the interpillar space and its internal surface area, respectively. It is important to remark that $\Omega_{\text{macro}}$ actually depends on the shape of the liquid-vapor interface $\Sigma_{lv}$, which, in turn, determines the solid-vapor one $\Sigma_{sv}$ and the vapor volume $V_v$. Since $\Omega_{\text{macro}}$ defined in Eq. (6) is a functional of the complete $\Sigma_{lv}$, it can be computed for arbitrarily complex configurations of the capillary system, e.g., along wetting paths which may or may not contain collective effects. The first term on the RHS corresponds to the bulk energy of a system containing a vapor bubble of volume $V_v$: at $\Delta P > 0$ vapor bubbles are energetically hindered while at negative pressures they are favored. This term is the driving force for the liquid-vapor transition. The second terms on the RHS are the energy costs of the liquid-vapor and solid-vapor interfaces, respectively; both are multiplied by the liquid-vapor surface tension $\gamma_{lv}$. The cost of $A_{sv}$ is modulated by the Young contact angle $\cos \theta_Y \equiv (\gamma_{sv} - \gamma_{sl})/\gamma_{lv}$ where $\gamma_{sv}$ and $\gamma_{sl}$ are the solid-vapor and the solid-liquid surface tensions, respectively. In the hydrophobic case considered here ($\theta_Y > \pi/2$), it is energetically favorable to increase $A_{sv}$, e.g., by dewetting the pillars: this is why at the liquid-vapor bulk coexistence ($\Delta P \approx 0$) the Cassie state is thermodynamically stable.
The terms in Eq. (6), which are needed in order to make a connection with the atomistic simulations, are consistent with the properties of the atomistic system and can be computed as follows (see Supplemental Material for details on the calculations of the contact angle, surface tension, and areas [36]). $\Delta P = 0.011 \varepsilon \sigma^{-3}$ is fixed, while $\gamma_{lv} = 0.57 \varepsilon \sigma^{-2}$ and $\theta_Y = 113^\circ$ are computed via independent MD simulations. The liquid-vapor and solid-liquid areas are computed by applying the marching cube method [45] on the $1 \times 1 \times 1 \sigma^3$ coarse-grained density field obtained from the string calculations. The volume of vapor is computed as $V_v \equiv (N_W - N)/(\rho_l - \rho_v)$, where $N_W$ and $N$ are the number of particles within the yellow region of Fig. 1 in the Wenzel and in a generic state, respectively, and $\rho_l$ and $\rho_v$ are the bulk liquid and vapor densities. It is important to remark that all the physical quantities are computed independently; i.e., they are not fitted to reproduce the atomistic free energy profile of wetting.

Figure 2(b) shows a fair agreement between the atomistic free energy and Eq. (6). In particular, the model in Eq. (6) does not include line tension, which is often invoked to explain in macroscopic terms nanoscale wetting phenomena [46,47]. One notices that the energetic difference between the atomistic and macroscopic models [dotted red curve of Fig. 2(b)] is a small fraction of the wetting barrier, $\approx 10\%$. This suggests that nanoscale effects, which include line tension, dependence of the surface tension on the curvature of the meniscus, width of the interfaces, etc., play a minor role in the transition path and kinetics of the wetting of the present system. In particular, considering that the contact line changes significantly in regimes III–V, the present results indicate that line tension does not change dramatically the free energy profile for hydrophobic pillars on the 3 nm scale, pushing further down the limit where line effects might be relevant (recent experimental work on superhydrophobicity [6] showed the same for textures down to 10 nm). More precisely, the combination of atomistic simulations with the continuum analysis entailed in Eq. (6) shows that the contribution of line tension to the intrusion or nucleation free energy barriers is negligible for the present system. It will be interesting to use a similar approach to explore extreme confinement (of the order of a nanometer or less), where a major contribution of line tension is expected [46].

The differences observed in the pinning region might be ascribed to the increased thickness of the area [36]).

Apart from these minor limitations, Eq. (6) provides a simple interpretation of the atomistic collapse mechanism shown in Fig. 2(a). In I, the area $A_{lv}$ of the liquid-vapor interface slightly increases, reflecting the increasing curvature due to pinning.

In II, $A_{lv}$ remains constant, while $A_{sv}$ linearly decreases, which corresponds to an increase of the interface area between the liquid and the hydrophobic solid. This surface term more than balances the decreasing bulk term $\Delta PV_v$, resulting in a linear increase of the free energy. If the interface were to keep this “flat” configuration until the bottom surface is fully wet, as assumed in classical works [41,48], the linear trend would continue, determining a much larger free energy barrier $\Delta \Omega_{cw}^1 = 920 k_B T$. This figure would lead, in turn, to estimate a lifetime of superhydrophobicity exponentially longer than for the mechanism shown in Fig. 2 (10^{108} times). Instead, at variance with the classical mechanism, at a distance $h_{TS} \approx 6 \sigma$ from the bottom surface (part III), it is energetically more convenient to bend the liquid-vapor interface between two pillars. The free energy of formation of this finger is seen to be negligible, while it allows the liquid to wet the bottom surface. Thus, the two liquid-vapor and vapor-solid interfaces are replaced by a single liquid-solid one, which decreases the total free energy by $\Omega_{dry} - \Omega_{wet} = \gamma_{lv}(A_{lv, dry} + \cos \theta_Y A_{sv, dry}) > 0$ [Fig. 2(c)].

C. Comparison with results in the literature

It is now possible to compare the path in Fig. 2 obtained via the atomistic string with those available in the literature and computed via continuum [15,22] and atomistic [7,14] simulations. Pashos et al. [22] considered a sharp interface model for the liquid-vapor interface with an empirical diffuse liquid-solid potential, which was introduced in order to simplify the numerical treatment of
complex textures and topological changes of the meniscus (for a similar approach, see Ref. [25]; see also the Supplemental Material for the effective diffuse liquid-solid potential computed via MD for the present solid-liquid interactions [36]). The pillar height-to-width ratio is very low, such that the surface is physically reminiscent of a naturally rough one rather than the artificial textures used for superhydrophobicity [6]. In particular, the interaction length of the liquid-solid potential is roughly half the pillar height. The path obtained with this model is still characterized by the formation of a liquid finger touching the bottom wall in a single point with the liquid front then moving to neighboring pillars. However, the free energy profile is very different from the present, with a number of intermediate transition states. This discrepancy is not unexpected, given the different pillars height and the different range of potentials employed.

Ren and coworkers [15,16] combined the string method with a mesoscale diffuse interface model in order to study the impalement of a drop on 3D surfaces with (slender) pillars. Although the system is rather different from the present one, the finger mechanism was found to be always energetically favorable. The finite lateral extent of the drop, however, significantly alters the latter stage of the Cassie-Wenzel transition.

Savoy and Escobedo [14] studied the Cassie-Wenzel transition of a nanodroplet on quasi-2D pillars. In their atomistic trajectories obtained via forward flux sampling (FFS) [49] the formation of a liquid finger can also be identified in some atomistic configurations. However, it is difficult to compare other details of the path and the energetics, because the FFS method only gives access to independent atomistic trajectories and not to the most probable density field as for the string.

Patel and coworkers [7] used umbrella sampling to study the collapse of the submerged superhydrophobic state on pillars. This geometry is very close to the present one, the main difference being that there is a single elementary cell was studied, which, due to the periodic boundary conditions, corresponds to the wetting of a single pillar. While a sort of finger formation is observed in correspondence of the transition state, the subsequent wetting process substantially differs from that in Fig. 2 in two respects. The first one is that the wetting process is discontinuous, with jumps in the density field between neighboring configurations. This is a known artifact ensuing from the use of a single collective variable [25] that cannot distinguish among bubble shapes enclosing the same volume $V_v$; a detailed analysis on the choice of the CVs will be object of an upcoming work. The second difference is the shape of the vapor bubbles during the later stage of the transition: the use of a single elementary cell imposes a symmetry to them which does not necessarily correspond to the most probable one.

Summarizing this analysis of available simulations, the formation of a liquid finger has been reported in a number of previous works dealing with both drops and submerged surfaces, tall and short posts [7, 11, 12, 14, 15, 22, 24]. There are, however, also relevant differences in the configuration of this transition state. Here the liquid finger forms between two pillars; in such a way the liquid-vapor interface bends only on two sides of the pillars, while the remaining sides become wet. This is energetically favorable because the cost of replacing a portion of the two liquid-vapor and solid-vapor interfaces with a solid-liquid interface is lower than that of increasing $\Delta \mu_v - \gamma_v \cos \theta_Y < \gamma_v$. Therefore it seems that the exact point where the finger forms and, consequently, where the transition state occurs, depends on the details of the confining geometry (in particular on the height-to-spacing ratio of the pillars) and on the chemistry of the surface.

In general terms, the presence of the bottom surface breaks the translational symmetry of the meniscus sliding along the pillars and thus imposes a change of topology to the vapor bubble. The local formation of a single, relatively narrow liquid finger is the energetically favored way to accomplish this transition. It is still an open question whether the finger should touch the bottom surface symmetrically or not, i.e., if two equivalent vapor bubbles are formed at the bottom of the two pillars confining the finger. For the 2D groove geometry, simulations have suggested that the asymmetric pathway is energetically favored because it allows the formation of a single vapor bubble in a corner [25, 38]. However, this finding does not exclude that other pathways are possible and might also be favored for other reasons (e.g., kinetic or inertial reasons). Indeed, recent experiments [50] on a similar geometry suggest that both pathways are possible. Moreover, recent string calculations [24]
underscore that in 2D grooves pathways with both symmetric and asymmetric bubbles are possible, with the latter having a slightly lower free energy barrier.

On pillared surfaces, careful analysis of the collapse of the superhydrophobic state by confocal microscopy [51] revealed the (abrupt) formation of vapor bubbles at one of the pillars’ lower corners, after the first contact with the bottom wall. This asymmetry in the last stage of the wetting process possibly indicates that the finger formation, which is too fast to be experimentally observed, was asymmetric too.

IV. CONCLUSIONS

In summary, rare-event atomistic simulations have provided a detailed description of the collapse of the superhydrophobic Cassie state on a nanopillared surface. This system is often encountered in experiments and serves as a prototype for wetting of interconnected cavities. Results have showed that the collapse proceeds in five stages: depinning of the liquid-vapor interface from the pillars’ corners; progressive wetting of the pillars via an almost flat, horizontal meniscus; formation of a liquid finger between two pillars which touches the bottom wall; progressive filling by a nonflat meniscus; absorption of a percolating network of low-density domains connecting pairs of pillars. This mechanism is very different from 2D grooves [25,27,48] and also from other 3D simulations [7] and could be captured only with state-of-the-art simulation techniques. On the one hand, results indicate that the system should be large enough to capture the local formation of a liquid finger and the progressive filling of the surrounding spaces. On the other hand, the number and choice of collective variables should allow one to resolve density changes in between the pillars. These caveats should be borne in mind for simulations of wetting: artifacts can conceal the actual collapse mechanism, affect the estimation of the free energy barriers and, with exponential sensitivity, of the collapse kinetics. The continuum analysis of the MD results entailed in Eq. (6) has allowed us to identify the different area and volume contributions to the free energy along the collapse, showing that line tension, evaporation and condensation, and other nanoscale effects are negligible in the present conditions. These results shed light on the wetting process of interconnected gas reservoirs which can open new perspectives in the design of nanotextures.

ACKNOWLEDGMENTS

The authors acknowledge fruitful discussion with Francesco Salvadore. The research leading to these results has received funding from the European Research Council under the European Union’s Seventh Framework Programme (FP7/2007-2013)/ERC Grant agreement No. 339446. We acknowledge PRACE for awarding us access to resource FERMI based in Italy at Casalecchio di Reno.

APPENDIX: THE STRING METHOD IN COLLECTIVE VARIABLES

Referring to the specialized literature for a complete derivation [30], a brief summary of the steps needed to obtain Eq. (2) is given below to provide the uninitiated reader with the basic conceptual framework of the string method in collective variables:

1. A system of stochastic differential equations in the phase space of the original microscopic system (the $6n_f$-dimensional space given by the vector of coordinates $\vec{r}$ and velocities, momenta expressed in mass reduced coordinates, $\vec{v} = \dot{\vec{r}}$) is devised whose statistically-steady solution follows the equilibrium probability distribution $m(\vec{r}, \vec{v})$ specified by the given ensemble [30]. Its configurational part is the distribution $m(\vec{r}) = \int d\vec{v} m(\vec{r}, \vec{v})$ in Eqs. (3) and (4).

2. The backward Kolmogorov equation (BKE) $Lq = 0$ associated with the system of stochastic differential equations is identified. BKE is a partial differential equation for the scalar quantity $q$ in the $6n_f$-dimensional phase space of the system. $L$ is a linear partial differential operator involving derivatives with respect to both $\vec{r}$ and $\vec{v}$, $L = L_{\vec{r}, \vec{v}}$. When BKE is solved with boundary conditions

034202-12
\( q(r, v) = 0 \) for \((r, v) \in A\) and \( q(r, v) = 1 \) for \((r, v) \in B\), where \( A \) and \( B \) are the two sets in phase space corresponding to the two metastable macroscopic states (Cassie and Wenzel, respectively) to be addressed, its solution provides the committor \( q(r, v) \), \( q \) gives the probability that the state \((r, v)\) will reach \( B \) (the products, in the chemical nomenclature) before reaching \( A \) (the reactants). The solution of the BKE satisfies a minimum principle for the functional \( I = \int m(r, v) L q \, dr \, dv \) under the given boundary conditions. The committor is the actual reaction coordinate of the transition from \( A \) to \( B \), and its level surfaces \( q(r, v) = q_0 \) are the loci of the microstates with the same progress of the reaction.

(3) It is assumed that the selected collective variable, namely, the coarse-grained density field \( \theta(r, x) \), provides a good description of the transition. As a consequence the transition is described as well by minimizing the restriction \( \tilde{I} \) of \( I \) to the space of functions \( f(\rho_1, \ldots, \rho_M) \) defined on the coarse-grained density field. This is tantamount to assuming \( q \approx f(\theta(r, x)) \). Two aspects are worth being noted: (a) the minimum of \( \tilde{I} \) is now searched in the space of functions of \( M \) variables, \( f(\rho_1, \ldots, \rho_M) \), rather than in that of functions \( q \) defined on the \( 6n_f \)-dimensional phase space. (b) The CVs are taken to depend only on the configuration of the particles and not on their velocities \( v \). As we shall immediately see, upon minimizing \( \tilde{I} \) with respect to \( \theta \), certain averages naturally emerge. The functional

\[
\tilde{I} = \int dr \, dv \, m(r, v) L f(\theta(r, x))
\]

where the pdf of the relevant ensemble is typically factorized, \( m(r, v) = m_v(v)m_r(r) \), and \( L_r \) is the part of \( L_{r,v} \) involves only derivatives with respect to the configuration \( r \). To proceed further, the explicit expression of \( L_r \) is needed. For the system we are considering it turns out to be \( L_r = v_1 \cdot \partial \partial r_1 \) (sum is implied on repeated indices). It follows

\[
\tilde{I} = \int dv \, m_v(v)v_1 \otimes v_1 \cdot \int dr \, m_r(r) \frac{\partial f}{\partial \theta_1} \otimes \frac{\partial f}{\partial \theta_j} = C \int dr \, m_r(r) \frac{\partial f}{\partial \theta_1} \cdot \frac{\partial f}{\partial \theta_j}
\]

where \( \Omega(\rho_1, \ldots, \rho_M) \) and \( g_{ij}(\rho_1, \ldots, \rho_M) \) have been defined in Eqs. (3) and (4), respectively. Note that \( \int dv \, m_v(v)v_1 = C \delta_{pl} \) since the velocity of particle \( p \) is independent from particle \( l \).

(4) The Euler-Lagrange equations for the restricted functional \( \tilde{I} \) are easily derived as

\[
\frac{\partial}{\partial \rho_i} \left( e^{-\beta \Omega(\rho_1, \ldots, \rho_M)} g_{ij} \frac{\partial f}{\partial \rho_j} \right) = 0
\]

and can be interpreted as the backward Kolmogorov equation of the stochastic differential equation

\[
\frac{d\rho_i}{d\tau} = -g_{ij} \frac{\partial \Omega}{\partial \rho_j} - \frac{1}{\beta} \frac{\partial g_{ij}}{\partial \rho_j} + \sqrt{\frac{2}{\beta}} g_{ij}^{1/2} \xi_j,
\]

where \( \xi_j \) is a white noise, \( \langle \xi_j \rangle = 0 \), \( \langle \xi_j(\tau) \xi_k(\tau') \rangle = \delta_{jk} \delta(\tau - \tau') \).

(5) When the thermal energy \( 1/\beta = k_B T \) is small with respect to the typical free energy variation along the path (of the order of the free energy barrier the system has to overcome to undergo the
transition which, for rare events, is always much larger than \( k_B T \) the leading term in \( k_B T \) is negligible and one is left with a stochastic dynamics in which the probability of a discrete path connecting the initial and final state is a product of Gaussian terms. One can, thus, search for the most probable among these paths, i.e., the path that the transition almost certainly follows:

\[
\frac{d\rho_i}{d\tau} = -g_{ij} \frac{\partial \Omega}{\partial \rho_j},
\]

with boundary conditions \( \rho_a \in a \) and \( \rho_b \in b \), being \( a \) and \( b \) the two sets in the space of coarse-grained density distributions which corresponds to the Cassie and the Wenzel state, respectively. The problem, as stated in the main text, cannot be easily solved by direct integration. Reparametrization of the curve \( \rho(x) \) in terms of the arc length \( \lambda \) yields Eq. (2) and the problem can be reinterpreted as the relaxation of a string \( \rho(x, \lambda) \) joining the two metastable states \( \rho(x, 0) = \rho_a \in a \) and \( \rho(x, 1) = \rho_b \in b \) towards the most probable path.

\[\textbf{References}\]

[1] A. Lafuma and D. Quéré, Superhydrophobic states, Nat. Mater. 2, 457 (2003).
[2] D. Quéré, Wetting and roughness, Annu. Rev. Mater. Res. 38, 71 (2008).
[3] J. P. Rothstein, Slip on superhydrophobic surfaces, Annu. Rev. Fluid. Mech. 42, 89 (2010).
[4] E. Martines, K. Seunarine, H. Morgan, N. Gadegaard, C. D. W. Wilkinson, and M. O. Richle, Superhydrophobicity and superhydrophilicity of regular nanopatterns, Nano Lett. 5, 2097 (2005).
[5] T. Verho, J. T. Korhonen, L. Sainiem, V. Jokinen, C. Bower, K. Franze, S. Franssila, P. Andrew, O. Ikkala, and R. H. A. Ras, Reversible switching between superhydrophobic states on a hierarchically structured surface, Proc. Natl. Acad. Sci. USA 109, 10210 (2012).
[6] A. Checco, B. M. Ocko, A. Rahman, C. T. Black, M. Tasinkevych, A. Giacomello, and S. Dietrich, Collapse and Reversibility of the Superhydrophobic State on Nanotextured Surfaces, Phys. Rev. Lett. 112, 216101 (2014).
[7] S. Prakash, E. Xi, and A. J. Patel, Spontaneous recovery of superhydrophobicity on nanotextured surfaces, Proc. Natl. Acad. Sci. USA 113, 5508 (2016).
[8] M. Amabili, A. Giacomello, S. Meloni, and C. M. Casciola, Unraveling the Salvinia paradox: Design principles for submerged superhydrophobicity, Adv. Mater. Interfaces 2, 1500248 (2015).
[9] A. Giacomello, M. Chinappi, S. Meloni, and C. M. Casciola, Geometry as a catalyst: How vapor cavities nucleate from defects, Langmuir 29, 14873 (2013).
[10] C. Ybert, C. Barentin, C. Cottin-Bizonne, P. Joseph, and L. Bocquet, Achieving large slip with superhydrophobic surfaces: Scaling laws for generic geometries, Phys. Fluids 19, 123601 (2007).
[11] A. Dupuis and J. M. Yeomans, Modeling droplets on superhydrophobic surfaces: Equilibrium states and transitions, Langmuir 21, 2624 (2005).
[12] H. Kusumaatmaja and J. M. Yeomans, Modeling contact angle hysteresis on chemically patterned and superhydrophobic surfaces, Langmuir 23, 6019 (2007).
[13] T. Koishi, K. Yasuoka, S. Fujikawa, T. Ebisuzaki, and X. C. Zeng, Coexistence and transition between Cassie and Wenzel state on pillared hydrophobic surface, Proc. Natl. Acad. Sci. USA 106, 8435 (2009).
[14] E. S. Savoy and F. A. Escobedo, Molecular simulations of wetting of a rough surface by an oily fluid: Effect of topology, chemistry and droplet size on wetting transition rates, Langmuir 28, 3412 (2012).
[15] W. Ren, Wetting transition on patterned surfaces: Transition states and energy barriers, Langmuir 30, 2879 (2014).
[16] Y. Zhang and W. Ren, Numerical study of the effects of surface topography and chemistry on the wetting transition using the string method, J. Chem. Phys. 141, 244705 (2014).
[17] G. Pashos, G. Kokkoris, and A. G. Boudouvis, Minimum energy paths of wetting transitions on grooved surfaces, Langmuir 31, 3059 (2015).
[18] A. Giacomello, S. Meloni, M. Chinappi, and C. M. Casciola, Cassie-Baxter and Wenzel states on a nanostructured surface: Phase diagram, metastabilities, and transition mechanism by atomistic free energy calculations, *Langmuir* **28**, 10764 (2012).

[19] E. S. Savoy and F. A. Escobedo, Simulation study of free-energy barriers in the wetting transition of an oily fluid on a rough surface with reentrant geometry, *Langmuir* **28**, 16080 (2012).

[20] M. Amabili, E. Lisi, A. Giacomello, and C. M. Casciola, Wetting and cavitation pathways on nanodecorated surfaces, *Soft Matter* **12**, 3046 (2016).

[21] A further advantage of the submerged setup is that results are also relevant for understanding the collapse of liquid drops with size much larger than the nanotexture.

[22] G. Pashos, G. Kokkoris, A. G. Papathanasiou, and A. G. Boudouvis, Wetting transitions on patterned surfaces with diffuse interaction potentials embedded in a Young-Laplace formulation, *J. Chem. Phys.* **144**, 034105 (2016).

[23] N. Tretyakov, P. Papadopoulos, D. Vollmer, H.-J. Butt, B. Dünnweg, and K. Ch. Daoulas, The Cassie-Wenzel transition of fluids on nanostructured substrates: Macroscopic force balance versus microscopic density-functional theory, *J. Chem. Phys.* **145**, 134703 (2016).

[24] J. R. Panter and H. Kusumaatmaja, The impact of surface geometry, cavitation, and condensation on wetting transitions: Posts and reentrant structures, *J. Phys. Condens. Matter* **29**, 084001 (2017).

[25] A. Giacomello, S. Meloni, M. Müller, and C. M. Casciola, Mechanism of the Cassie-Wenzel transition via the atomistic and continuum string methods, *J. Chem. Phys.* **142**, 104701 (2015).

[26] R. Evans and M. C. Stewart, The local compressibility of liquids near non-adsorbing substrates: A useful measure of solvophobicity and hydrophobicity? *J. Phys. Condens. Matter* **27**, 194111 (2015).

[27] J. De Coninck, F. Dunlop, and T. Huillet, Metastable wetting, *J. Stat. Mech.* (2011) P06013.

[28] S. Bonella, S. Meloni, and G. Ciccotti, Theory and methods for rare events, *Eur. Phys. J. B* **85**, 97 (2012).

[29] T. Lelièvre, G. Stoltz, and M. Rousset, *Free Energy Computations a Mathematical Perspective* (World Scientific, London, 2010), p. 472.

[30] L. Maragliano, A. Fischer, E. Vanden-Eijnden, and G. Ciccotti, String method in collective variables: Minimum free energy paths and isocommittor surfaces, *J. Chem. Phys.* **125**, 024106 (2006).

[31] T. F. Miller, E. Vanden-Eijnden, and D. Chandler, Solvent coarse-graining and the string method applied to the hydrophobic collapse of a hydrated chain, *Proc. Natl. Acad. Sci. USA* **104**, 14559 (2007).

[32] R. Evans, Density functionals in the theory of nonuniform fluids, in *Fundamentals of Inhomogeneous Fluids*, edited by D. Henderson (Marcel Dekker, New York, 1992), Chap. 3, p. 85.

[33] H. Löwen, Density functional theory of inhomogeneous classical fluids: Recent developments and new perspectives, *J. Phys. Condens. Matter* **14**, 11897 (2002).

[34] E. Weinan, W. Ren, and E. Vanden-Eijnden, Simplified and improved string method for computing the minimum energy paths in barrier-crossing events, *J. Chem. Phys.* **126**, 164103 (2007).

[35] L. Maragliano and E. Vanden-Eijnden, A temperature accelerated method for sampling free energy and determining reaction pathways in rare events simulations, *Chem. Phys. Lett.* **426**, 168 (2006).

[36] See Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevFluids.2.034202 for simulation details.

[37] G. J. Martyna, M. L. Klein, and M. Tuckerman, Nosé-Hoover chains: the canonical ensemble via continuous dynamics, *J. Chem. Phys.* **97**, 2635 (1992).

[38] A. Giacomello, M. Chinappi, S. Meloni, and C. M. Casciola, Metastable Wetting on Superhydrophobic Surfaces: Continuum and Atomistic Views of the Cassie-Baxter–Wenzel Transition, *Phys. Rev. Lett.* **109**, 226102 (2012).

[39] M. Amabili, A. Giacomello, S. Meloni, and C. M. Casciola, Intrusion and extrusion of a liquid on nanostructured surfaces, *J. Phys. Condens. Matter* **29**, 014003 (2017).

[40] S. Plimpton, Fast parallel algorithms for short-range molecular dynamics, *J. Comput. Phys.* **117**, 1 (1995).

[41] N. A. Patankar, Consolidation of hydrophobic transition criteria by using an approximate energy minimization approach, *Langmuir* **26**, 8941 (2010).

[42] See Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevFluids.2.034202 for a video of the wetting transition.
[43] The quasistatic assumption also implies that the effect of viscosity and other kinetic effects are neglected in the present approach.

[44] K. Kelton and A. L. Greer, *Nucleation in Condensed Matter: Applications in Materials and Biology* (Pergamon, Amsterdam, 2010).

[45] W. E. Lorensen and H. E. Cline, Marching cubes: A high resolution 3D surface construction algorithm, in *Proceedings of the 14th Annual Conference on Computer Graphics and Interactive Techniques*, SIGGRAPH ’87 (ACM, New York, 1987), Vol. 21, p. 163.

[46] S. Sharma and P. G. Debenedetti, Evaporation rate of water in hydrophobic confinement, *Proc. Natl. Acad. Sci. USA* 109, 4365 (2012).

[47] L. Guillemot, T. Biben, A. Galarneau, G. Vigier, and É. Charlaix, Activated drying in hydrophobic nanopores and the line tension of water, *Proc. Natl. Acad. Sci. USA* 109, 19557 (2012).

[48] N. A. Patankar, On the modeling of hydrophobic contact angles on rough surfaces, *Langmuir* 19, 1249 (2003).

[49] R. J. Allen, C. Valeriani, and P. R. ten Wolde, Forward flux sampling for rare event simulations, *J. Phys. Condens. Matter* 21, 463102 (2009).

[50] P. Lv, Y. Xue, H. Liu, Y. Shi, P. Xi, H. Lin, and H. Duan, Symmetric and asymmetric meniscus collapse in wetting transition on submerged structured surfaces, *Langmuir* 31, 1248 (2015).

[51] P. Papadopoulos, L. Mammen, X. Deng, D. Vollmer, and H.-J. Butt, How superhydrophobicity breaks down, *Proc. Natl. Acad. Sci. USA* 110, 3254 (2013).