LETTER

A CNN-Based Optimal CTU $\lambda$ Decision for HEVC Intra Rate Control

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SUMMARY Since HEVC intra rate control has no prior information to rely on for coding, it is a difficult work to obtain the optimal $\lambda$ for every coding tree unit (CTU). In this paper, a convolutional neural network (CNN) based intra rate control is proposed. Firstly, a CNN with two last output channels is used to predict the key parameters of the CTU $\lambda$-curve. For well training the CNN, a combining loss function is built and the balance factor $\gamma$ is explored to achieve the minimum loss result. Secondly, the initial CTU $\lambda$ can be calculated by the predicted results of the CNN and the allocated bit per pixel (bpp). According to the rate distortion optimization (RDO) of a frame, a spatial equation is derived between the CTU $\lambda$ and the frame $\lambda$. Lastly, The CTU clipping function is used to obtain the optimal CTU $\lambda$ for the intra rate control. The experimental results show that the proposed algorithm improves the intra rate control performance significantly with a good rate control accuracy.

key words: HEVC, intra rate control, CNN, rate distortion optimization

1. Introduction

Rate control is mainly used to achieve optimal quality of the coding video under the given target bit rate. For high-efficiency video coding (HEVC), the $\lambda$ domain rate control [1] builds a typical relationship between the Lagrange multiplier, the bit per pixel (bpp) and the rate control parameters. For $\lambda$ domain rate control, some researches studied on the the CTU level [2] and the frame level [3] bit allocation. Additionally, a separated $\lambda$ decision algorithm [4] was proposed for the surveillance videos.

However, as the intra rate control has a significant effect on the following frames, it is an important work to improve the intra coding performance. Wang et al. [5] allocated bpp of intra CTU according to the gradient per pixel (gpp), but the bpp assigned by the traditional method was difficult to satisfy the CTU spatial coding feature. Therefore, the convolutional neural network (CNN)-based intra rate control has been proposed that achieves an outstanding performance. Santamaria et al. [6] gave the bit and distortion prediction for intra rate control by two CNNs. Lu et al. [7] predicted the coefficients of the R-Quantization model by a designed CNN. As Li et al. [8] suggested that QP was not suitable for the flexible coding structure of HEVC which indicated that using QP as the key factor for rate control would limit coding performance. In [9], two CNNs were used to predict two parameters of the R-$\lambda$ curve. However, it ignored the whole coding performance of a frame and the predicted $\lambda$ might be singular. Therefore, it is necessary to explore the spatial relationship of every CTU $\lambda$ for the reasonable coding in a whole frame.

As intra rate control has little prior coding information, it is difficult to improve intra coding quality under a high control accuracy. In this paper, a designed CNN is used to predict the key parameter of the R-$\lambda$ relationship. To minimize the training loss of the CNN, a combining loss function is built and the balance factor $\gamma$ is explored. Then, with the rate distortion optimization (RDO) process, a spatial equation of the CTU $\lambda$ and the frame $\lambda$ can be derived. Lastly, according to the RDO derivation, a special clipping method is used to obtain the optimal CTU $\lambda$ for coding the whole frame reasonably.

2. Proposed CNN-Based Optimal CTU $\lambda$ Decision

2.1 R-$\lambda$ Relationship of CTU

We ran the HEVC encoder numerous times to observe the R-$\lambda$ characteristics of different CTUs with QP = 22, 27, 32 and 37 respectively at all intra configuration. The experimental results are shown in Fig. 1.

It is observed from Fig. 1 that the R-$\lambda$ curve of a CTU obeys the hyperbolic function that can be modeled as

$$\lambda = \alpha \cdot R^{-\beta}$$  \hspace{1cm} (1)

where $\alpha$ and $\beta$ are the key model parameters. $R$ is mod-

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Fig. 1 R-$\lambda$ curves for (a) the 6th CTU in BasketballDrill at the 1st frame, (b) the 10th CTU in PartyScene at the 1st frame
eled by bpp. We also observe that different CTUs have quite different R-\(\lambda\) characteristics from each other. On the other hand, if the accurate R-\(\lambda\) curve of a CTU can be obtained prior to coding, it will achieve the optimal coding performance with any allocated bpp as long as the R-\(\lambda\) point is located on the curve.

2.2 CNN-Based CTU R-\(\lambda\) Prediction

As described by Eq. (1), we use the CNN to predict \(\alpha\) and \(\beta\). We pick out approximately 5000 frames from different kinds of sequences. To reduce the correlation of the adjacent frames, ten frames that consist of the first frame and nine frames of the integer multiple of the frame rate after the first frame are selected from every sequence. Every frame is compressed by HEVC for all intra configuration with QP = 22, 27, 32 and 37. Every CTU in a single image will have four points, and then the R-\(\lambda\) curve of the CTU will be fitted by the four points to obtain \(\alpha\) and \(\beta\) in Eq. (1). We obtain statistics for \(\alpha\) and \(\beta\) from 300000 R-\(\lambda\) curves, with the results shown in Figs. 2 (a) and (b), respectively.

In Figs. 2 (a) and (b), the horizontal axis represents the values of \(\alpha\) and \(\beta\), respectively, and the vertical axis represents the number of the CTUs used for training. \(x_n\) and \(y_n\) are the prediction of \(\alpha\) and \(\beta\) from the CNN, respectively. \(X_n\) and \(Y_n\) are the ground truth of \(\alpha\) and \(\beta\), respectively. \(\gamma\) is the balance factor. The training is performed by stochastic gradient descent with standard back-propagation.

For training the CNN, \(\gamma\) is changed to explore the Combining loss result. We set the maximum number of training iterations to 1500000 and observe that after approximately 1100000 iterations, the training and testing loss results tend to be stable. The Combining loss results with different \(\gamma\) are shown in Fig. 4.

From Fig. 4, it can be seen that the combining loss has the smallest value, which is nearly to 1.87, when \(\gamma\) equals to 1. Therefore, we obtain \(\alpha\) and \(\beta\) for Eq. (1) from the CNN which is trained with the combining loss function as \(\gamma\) equals to 1.

2.3 Optimal CTU \(\lambda\) Decision

To minimize the distortion for the intra rate control, the RDO problem of a frame can be modeled as

\[
\min_{[r_{CTU}(i)]_{i=1}^{N_{CTU}}} D_F = \sum_{i=1}^{N_{CTU}} d_{CTU}(i)
\]

s.t. \(R_F = \sum_{i=1}^{N_{CTU}} r_{CTU}(i) \leq T_F\) \hspace{1cm} (3)

where \(D_F\) and \(R_F\) are the distortion and the bit rate of the current frame, respectively. \(N_{CTU}\) is the number of CTUs in the current frame. \(T_F\) is the target bit rate. Then, the Lagrange multiplier method can be converted to an equivalent unconstrained problem as

\[
\min_{[r_{CTU}(i)]_{i=1}^{N_{CTU}}} \sum_{i=1}^{N_{CTU}} d_{CTU}(i) + \lambda_F \cdot \sum_{i=1}^{N_{CTU}} r_{CTU}(i) \hspace{1cm} (4)
\]

where \(z \in [1, N_{CTU}]\) and \(\lambda_F\) is the Lagrange multiplier of the current frame. Then, Eq. (4) can be solved by setting its derivative to zero,

\[
\frac{\partial}{\partial r_{CTU}(i)} \sum_{i=1}^{N_{CTU}} d_{CTU}(i) + \lambda_F \frac{\partial}{\partial r_{CTU}(i)} \sum_{i=1}^{N_{CTU}} r_{CTU}(i) = 0 \hspace{1cm} (5)
\]

As every CTU is encoded separately for intra rate control. Taking \(\lambda_{CTU}(i) = -\partial d_{CTU}(i)/\partial r_{CTU}(i)\) into Eq. (5), we can obtain,
\[ \sum_{i=1}^{N_{CTU}} \lambda_{CTU}(i) / N_{CTU} = \lambda_f \] (6)

where Eq. (6) indicates that the mean \( \lambda \) of the CTUs in a frame should be equal to the current frame \( \lambda \). As all the CTUs cannot be obtained once for calculating the final mean \( \lambda \) in Eq. (6), a clipping method is used to make the mean \( \lambda \) of the encoded CTUs tend to the frame \( \lambda \), which is defined as

\[
\text{clip}[\max(\sum_{u=1}^{i-1} \lambda_{CTU}(u)/(i - 1) \cdot a, \lambda_f \cdot a, \lambda_f)] \\
\min(\sum_{u=1}^{i-1} \lambda_{CTU}(u)/(i - 1) \cdot b, \lambda_f \cdot b, \lambda_{CTU}(i))
\] (7)

where \( a \) and \( b \) are the empirical values which are \( 2^{-1/3} \) and \( 2^{1/3} \), respectively. In Eq. (7), \( \lambda_{CTU}(i) \) of \( i \)-th encoding CTU is affected not only by the frame \( \lambda \) but also by the mean CTU \( \lambda \) of the encoded CTUs. Thus, Eq. (6) can be approximately satisfied.

### 3. Experimental Results

The proposed algorithm is implemented into HM16.9. The default intra rate control method, which are the CTU level (HMMode1) and frame level rate control (HMMode2), of HM16.9 and the intra rate control of Li et al. [9] are used for comparison. It should be noted that we use our data set for training the CNNs which are proposed in [9], and turn off rate control to compress the first frame with QP = 22, 27, 32 and 37, then use the resulting bit rates as the target bit rates. We follow the HEVC common test conditions with 15 test sequences. The bit rate accuracy is defined as

\[ M = |T_{\text{actual}} - T_{\text{target}}| / T_{\text{target}} \] (8)

where \( T_{\text{actual}} \) is the actual bit rate. \( T_{\text{target}} \) is the target bit rate.

The bit rate accuracy results are shown in Table 1. It is observed from Table 1 that the average bit rate accuracy results of the four algorithm are 1.61\%, 2.21\%, 5.75\% and 13.06\%, respectively. Since the average bit rate accuracy of HMMode2 is much worse than those of the other algorithms, it is inconsistent with the main purpose of the rate control. On the other hand, control of the bit rate is a highly challenging task for intra coding with only one frame. The accuracies of the proposed algorithm, the algorithm of Li et al. [9] and HMMode1 remain high.

We use HMMode1, HMMode2 and the algorithm of Li et al. [9] as the comparison respectively to obtain the BDRate and BDPSNR results, which are shown in Table 2. An examination of the data presented in Table 2 shows that the average BDRate and BDPSNR of the proposed algorithm and HMMode1 are \(-1.36\% \) and \(0.07\) dB. This means that the proposed algorithm always uses less bit rate, but improves the coding quality. For the comparison of the proposed algorithm and the algorithm of Li et al. [9], the BDRate is decreased by \(2.28\% \) and the BDPSNR is increased by \(0.13\) dB. The proposed algorithm has a better coding performance mainly about two reasons, the first one is that a deeper CNN structure is used which will lead to a more accurate prediction and the calculated \( \lambda \) is more suitable for every CTU. The other one is that every CTU is clipped together and the whole frame can be coded reason-

### Table 1 Bit rate accuracy results of HMMode1, the algorithm of Li et al. [9], the proposed algorithm and HMMode2

| Sequences | HMMode1 M% | Li et al. [9] M% | Proposed M% | HMMode2 M% |
|-----------|------------|-----------------|-------------|------------|
| Class A   | 3.01       | 5.22            | 8.50        | 15.33      |
| Class B   | 1.41       | 1.40            | 6.27        | 12.88      |
| Class C   | 1.04       | 1.03            | 4.40        | 12.52      |
| Class D   | 0.95       | 1.16            | 3.83        | 11.53      |
| Average   | 1.61       | 2.21            | 5.75        | 13.06      |

### Table 2 Experimental comparison results for the proposed algorithm with HMMode1, the algorithms of Li et al. [9] and HMMode2

| Sequences   | Proposed versus HMMode1 BDRate | Proposed versus HMMode1 BDPSNR | Proposed versus Li et al. [9] BDRate | Proposed versus Li et al. [9] BDPSNR | Proposed versus HMMode2 BDRate | Proposed versus HMMode2 BDPSNR |
|-------------|--------------------------------|--------------------------------|--------------------------------------|--------------------------------------|--------------------------------|--------------------------------|
| Class A     | PeopleOnStreet -0.86 0.05      | -1.82 0.10                     | 2.36 -0.13                           | 2.79 -0.15                           |
|             | Traffic -1.10 0.06           | -2.29 0.13                     | 2.57 -0.14                           | 2.89 -0.14                           |
|             | BasketballDrive -2.37 0.06    | -2.30 0.05                     | 2.64 -0.07                           | 2.97 -0.08                           |
|             | BQTerrace -1.84 0.11         | -3.06 0.19                     | 4.04 -0.23                           | 4.36 -0.24                           |
| Class B     | Cactus -2.36 0.09           | -3.58 0.14                     | 5.13 -0.19                           | 5.49 -0.19                           |
|             | Kimono -1.42 0.05            | -2.49 0.09                     | 2.78 -0.10                           | 3.09 -0.11                           |
|             | ParkScene -1.79 0.08         | -2.55 0.11                     | 3.23 -0.10                           | 3.55 -0.11                           |
|             | BasketballDrill -2.08 0.10   | -2.41 0.11                     | 2.56 -0.12                           | 2.88 -0.12                           |
|             | BGColor -1.07 0.07           | -2.12 0.14                     | 2.97 -0.18                           | 3.29 -0.19                           |
| Class C     | PartyScene -0.56 0.05        | -0.75 0.06                     | 0.48 -0.03                           | 0.76 -0.03                           |
|             | RaceHorses -1.20 0.08        | -1.85 0.12                     | 1.87 -0.12                           | 2.19 -0.13                           |
|             | BasketballPass -0.68 0.04    | -1.87 0.12                     | 3.05 -0.19                           | 3.37 -0.19                           |
| Class D     | BlowingBubbles -0.60 0.03    | -0.73 0.04                     | 1.11 -0.06                           | 1.43 -0.07                           |
|             | BQSquare -0.63 0.05          | -3.40 0.29                     | 4.36 -0.36                           | 4.69 -0.37                           |
|             | RaceHorses -1.86 0.14        | -2.99 0.21                     | 3.55 -0.24                           | 3.89 -0.25                           |
| Average     | -1.36 0.07                   | -2.28 0.13                     | 2.79 -0.15                           | 3.12 -0.17                           |
ably. With the comparison of HMMode2, the BDRate increases 2.79 and the BDPSNR decreases 0.15. However, HMMode2 sacrifices too much rate control accuracy which does not satisfy the purpose of intra rate control. Therefore, the proposed algorithm has the better rate control performance than the other algorithms. Some subjective comparisons are shown in Fig. 5.

It is observed from Fig. 5 (a-2) that the number 6 on the clock is missing as well as that in Fig. 5 (a-3). However, the proposed algorithm, which can be seen in Fig. 5 (a-4), has a clear result in the same region. Similarly, the subjective qualities of the face regions presented in Figs. 5 (b-2) and (b-3) are worse than that of the image in Fig. 5 (b-4). Since the intra rate control frame will be referred by the following frames, it is important to improve the intra coding quality as much as possible under the target bit rate.

4. Conclusions

In this paper, a CNN-based intra rate control is proposed. Firstly, a CNN is designed to predict CTU $\lambda$-R relationship. Then, the combining loss function with the balance factor $\gamma$ is built for training the CNN. Secondly, the CTU $\lambda$ can be obtained by the training results and the allocated bpp. However, the calculated $\lambda$ is not suitable for coding. Then, with the RDO process of a frame, the spatial equation relationship of the CTU $\lambda$ and the frame $\lambda$ can be derived. Lastly, the spatial limitation of every CTU in a frame is built for the reasonable coding of the whole frame. For the experimental results, the proposed algorithm has a better rate control performance than the comparison algorithms.

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