Measurement of $D^0\bar{D}^0$ Mixing using the Ratio of Lifetimes for the Decays $D^0 \to K^+\pi^- + K^-K^+$

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We measure the rate of $D^0$-$\bar{D}^0$ mixing with the observable $y_{\text{CP}} = (\tau_{K\pi} / \tau_{KK}) - 1$, where $\tau_{K\pi}$ and $\tau_{KK}$ are respectively the mean lifetimes of CP-even $D^0 \to K^+ K^-$ and CP-mixed $D^0 \to K^- \pi^+$ decays, using a data sample of 384 fb$^{-1}$ collected by the BaBar detector at the SLAC PEP-II asymmetric-energy B Factory. From a sample of $D^0$ and $\bar{D}^0$ decays where the initial flavor of the decaying meson is not determined, we obtain $y_{\text{CP}} = [1.12 \pm 0.26(\text{stat}) \pm 0.22(\text{syst})] \%$, which excludes the no-mixing hypothesis at 3.8$\sigma$, including both statistical and systematic uncertainties. This result is in good agreement with a previous BaBar measurement of $y_{\text{CP}}$ obtained from a sample of $D^{\ast+} \to D^0 \pi^+$ events, where the $D^0$ decays to $K^- \pi^+$, $K^+ K^-$, and $\pi^+ \pi^-$, which is disjoint with the untagged $D^0$ events used here. Combining the two results taking into account statistical and systematic uncertainties, where the systematic uncertainties are assumed to be 100% correlated, we find $y_{\text{CP}} = [1.16 \pm 0.22(\text{stat}) \pm 0.18(\text{syst})] \%$, which excludes the no-mixing hypothesis at 4.1$\sigma$.

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Several recent results [1, 2, 3, 4] show evidence for mixing in the $D^0\bar{D}^0$ system consistent with predictions of possible Standard Model contributions [5, 6, 7, 8, 9]. These results also constrain many new physics models [10, 11, 12, 13, 14], and increasingly precise $D^0\bar{D}^0$ mixing measurements will provide even stronger constraints. One manifestation of $D^0\bar{D}^0$ mixing is differing $D^0$ decay time distributions for decays to different CP eigenstates [15]. We present here measurement of this lifetime difference using a sample of $D^0$ and $\bar{D}^0$ decays in which the initial flavor of the decaying meson is unknown.

Assuming CP conservation in mixing, the two neutral charm mass eigenstates $|D_1\rangle$ and $|D_2\rangle$ can be represented as

$$
|D_1\rangle = p|D^0\rangle + q|\bar{D}^0\rangle,
|D_2\rangle = p|D^0\rangle - q|\bar{D}^0\rangle,
$$

where $p^2 + q^2 = 1$. The rate of $D^0\bar{D}^0$ mixing can be characterized by the parameters $x = \Delta m/\Gamma$ and $y = \Delta \Gamma/2\Gamma$, where $\Delta m = m_1 - m_2$ and $\Delta \Gamma = \Gamma_1 - \Gamma_2$ are respectively the differences between the mass and width eigenvalues of the states in Eq. (1), and $\Gamma = (\Gamma_1 + \Gamma_2)/2$ is the average width. If either $x$ or $y$ is non-zero, mixing will occur, altering the decay time distribution of $D^0$ and $\bar{D}^0$ mesons decaying into final states of specific CP [16].

In the limit of small mixing, and no CP violation in mixing or in the interference between mixing and decay (assumptions which are consistent with current experimental results), the mean lifetimes of decays to a CP eigenstate of a sample of $D^0$ ($\tau_{hh}^{D^0}$) and $\bar{D}^0$ ($\tau_{hh}^{\bar{D}^0}$), along with the mean lifetime of decays to a state of indefinite CP ($\tau_{K\pi}$), can be combined into the quantity

$$
y_{CP} = \frac{\langle \tau_{K\pi} \rangle}{\langle \tau_{hh} \rangle} - 1, \tag{2}
$$

where $\langle \tau_{hh} \rangle = (\tau_{hh}^{D^0} + \tau_{hh}^{\bar{D}^0})/2$. Noting that the untagged $K^-\pi^+$ final state is a mixture of Cabibbo-favored and doubly Cabibbo-suppressed $D^0$ and $\bar{D}^0$ decays with a purely exponential lifetime distribution, along with a very small admixture of mixed $D^0$ decays, an analogous expression also holds for $\langle \tau_{K\pi} \rangle$. Given the current experimental evidence indicating a small mixing rate, the lifetime distribution for all $hh$ and $K\pi$ final states is exponential to a good approximation. If $y_{CP}$ is zero there is no $D^0\bar{D}^0$ mixing attributable to a width difference, although mixing caused by a mass difference may be present. In the limit of no direct CP violation, $y_{CP} = y$.

We measure the $D^0$ mean lifetime in the $D^0$ decay modes $K^-\pi^+$ and $K^+K^-$, where the initial flavor of the decaying $D^0$ is not identified (the untagged sample). This sample excludes $D^0$ mesons which can be reconstructed as part of $D^{*-} \rightarrow D^0\pi^-$ decays, as these decays (the tagged sample) are the subject of an earlier BABAR analysis [18] whose results are combined with those of the current analysis. To avoid potential bias, we finalized our data selection criteria, fitting methodology, sources of possible systematic uncertainties to be examined, and method of calculating statistical limits for the current untagged analysis alone and in combination with the tagged analysis, prior to examining the mixing results from the untagged data. In general, systematic uncertainties related to the reconstruction of signal events cancel in the lifetime ratio. However, uncertainties related to the somewhat differing backgrounds present in the $K^-\pi^+$ and $K^+K^-$ final states lead to larger systematic uncertainties in the untagged analysis compared to those of the tagged analysis, which has much higher signal purity.

We use 384 fb$^{-1}$ of $e^+e^-$ colliding-beam data recorded at, and slightly below, the $\Upsilon(4S)$ resonance (center-of-mass [CM] energy $\sqrt{s} \sim 10.6$ GeV) with the BABAR detector [19] at the SLAC National Accelerator Laboratory PEP-II asymmetric-energy B Factory. Candidate $D^0$ signal decays are reconstructed in the final states $K^-\pi^+$ and $K^+K^-$. The selection of events and reconstruction of $D^0$ signal candidates closely follows that of our previous tagged analysis [18]. We require $K^+$ and $\pi^+$ candidates to satisfy particle identification criteria based on $dE/dx$ ionization energy loss and Cherenkov angle measurements. We fit oppositely charged pairs of these candidates with appropriate mass hypotheses to a common vertex to form a $D^0$ candidate. The decay time $t$ of each $D^0$ candidate with invariant mass within the range $1.80 - 1.93$ GeV/$c^2$, along with its estimated uncertainty $\sigma_t$, is determined from a combined fit to the $D^0$ production and decay vertices, with a constraint that the production point be consistent with the $e^+e^-$ interaction region as determined on an event-by-event basis. We retain only candidates with a $\chi^2$-based probability for the fit $P(\chi^2) > 0.1\%$, and with $-2 < t < 4$ ps and $\sigma_t < 0.5$ ps.

We further require the helicity angle $\theta_H$, defined as the angle between the positively charged track in the $D^0$ rest frame and the $D^0$ direction in the laboratory frame, to satisfy $|\cos \theta_H| < 0.7$, which aids in the rejection of purely combinatorial background events. Contributions from true $D^0$ mesons produced in $B$ meson decay are reduced to a negligible amount by rejecting $D^0$ candidates with momentum in the $e^+e^-$ CM frame less than 2.5 GeV/$c$. For events with multiple candidates sharing one or more tracks, we retain only the candidate with the highest $P(\chi^2)$. The fraction of events with multiple signal candidates is $\sim 0.05\%$ for the $K^+K^-$ final state, and $\sim 0.3\%$ for $K^-\pi^+$.

The invariant mass distributions for the final $D^0 \rightarrow K^-\pi^+$ and $D^0 \rightarrow K^+K^-$ samples are shown in Fig. 1. For the lifetime fits, we use only events within $\pm 10$ MeV/$c^2$ of the $D^0$ signal peak 1.8545 $< M_{D^0} < 1.8745$ GeV/$c^2$ (the lifetime fit mass region). The $K^-\pi^+$ and $K^+K^-$ signal yields within this region and their purity are given in Table I. Events within the mass sideband regions 1.81 $< M_{D^0} < 1.83$ GeV/$c^2$ and 1.90 $< M_{D^0} < 1.92$ GeV/$c^2$ are used to determine the combinatorial background decay time distribution within the lifetime fit mass region. In addition to purely combinatorial backgrounds, there are small background contributions from decays of non-signal charm parents where two of the decay products are selected as the daughters of a signal decay and subsequently pass the final event selection. These misconstructed charm backgrounds are accounted for using simulated events. Their contribution is $\sim 0.7\%$ ($\sim 3.8\%$) of the total number of background events in the $K^-\pi^+$ ($K^+K^-$)
The mean $D^0$ lifetime is determined from a fit essentially identical to the one performed in the previous tagged analysis [18], using the reconstructed decay time $t$ and the decay time uncertainty $\sigma_t$ for events within the lifetime fit mass region. Three categories of events are accounted for in the lifetime fit: signal decays, combinatorial background, and misreconstructed charm events.

The decay time distribution of signal events is described by an exponential convolved with a resolution function which is taken as the sum of three Gaussian functions with widths proportional to $\sigma_t$. The functional form of this probability density function (PDF) for signal events is

$$R_X(t, \sigma_t; \tau_X) = f_{1\sigma}D(t, \sigma_t; S_X s_3, t_0, \tau_X) + (1 - f_{1\sigma}) \left[ f_{2\sigma}D(t, \sigma_t; S_X s_2, t_0, \tau_X) + (1 - f_{2\sigma})D(t, \sigma_t; S_X s_1, t_0, \tau_X) \right],$$

where $f_{1\sigma}$ (with $i = 1 \ldots 3$) parameterizes the contribution of each individual resolution function, $s_i$ is a scaling factor associated with each Gaussian, $\tau_X$ (where $X = K \pi$, $K\bar{K}$) is the lifetime parameter determined by the fit, $t_0$ is an offset to the mean of the resolution function, and where

$$D(t, \sigma_t; s, t_0, \tau) =$$

$$C_{\sigma_t} \int \exp \left( -t_{\text{true}}/\tau \right) \exp \left( \frac{-(t - t_{\text{true}} + t_0)^2}{2(s^2/\sigma_t^2)} \right) dt_{\text{true}}$$

with normalization coefficient $C_{\sigma_t}$. Up to an overall scale factor in the width, the resolution function is identical for both final states. We account for a small ($\sim 1\%$) difference in the $K^-\pi^+ + K^+K^-\pi^0$ and $K^+K^-\pi^0$ resolution function width using an additional fixed scale factor $S_X$. The value of $S_{KK}$ is determined from the data, with $S_{K\pi}$ fixed to 1.0. Possible biases resulting from this assumption are included as part of the study of systematic uncertainties. All other resolution function parameters are shared among the two modes, and all parameters are allowed to vary in a simultaneous extended unbinned maximum likelihood fit to both final states.

The decay time distribution of the combinatorial background is described by a sum of two Gaussians and a modified Gaussian with a power-law tail to account for a small number of events with large reconstructed lifetimes. The widths of these Gaussians are not scaled using event-by-event uncertainties. Events in the lower and upper $K^-\pi^+ (K^+K^-)$ mass sidebands are fit separately, and a weighted average of the results of these fits is used to parameterize the PDF for $K^-\pi^+ (K^+K^-)$ combinatorial events in the lifetime fit mass region.

Misreconstructed charm background events have one or more of the charm decay products either not reconstructed or reconstructed with the wrong particle hypothesis. In the $K^-\pi^+ (K^+K^-)$ final state, $\sim 60\%$ ($\sim 95\%$) of these events are from true $D^0$ decays, with the balance coming from charged $D$ and charm baryon decays. The charm background is long-lived and is described using an exponential convolved with a resolution function consisting of two Gaussians with a shared mean and widths that depend on $\sigma_t$. Because the number of these events in the $K^-\pi^+ (K^+K^-)$ sample is small relative to the total background, an effective lifetime distribution taken from simulated events and summed over all $K^-\pi^+ (K^+K^-)$ charm backgrounds is used in the $K^-\pi^+ (K^+K^-)$ lifetime fit.

Since the lifetime fit PDFs depend on the event-by-event decay time uncertainty, PDFs describing the distribution of decay time uncertainties for each of the event classes are required to avoid bias in the likelihood estimator used in the data fit [20]. We extract these distributions directly from the data. For combinatorial events, the distribution of decay time uncertainties is taken from a weighted average of the distributions extracted from the lower and upper mass sidebands. The decay time uncertainty distribution for signal events is obtained by subtracting the combinatorial background uncertainty distribution from the uncertainty distribution of all (i.e., background plus signal) candidates present in the lifetime fit mass region. The signal distribution is also used for the relatively small number of misreconstructed charm background events.

The results of the lifetime fits are shown in Figs. 2 and 3 along with a plot of the point-by-point residuals for each fit normalized by the statistical uncertainty associated with a data point. We find the $D^0 \to K^-\pi^+$ mean lifetime $\tau_{K\pi} = 410.39 \pm 0.38(\text{stat})$ fs and the $D^0 \to K^+K^-$ mean lifetime $\tau_{KK} = 405.85 \pm 1.00(\text{stat})$ fs, yielding $y_{CP} = [1.12 \pm 0.26(\text{stat})]\%$. The statistical significance of this mixing result without taking into account systematic uncertainties is $4.3\sigma$. This untagged result is in good agreement with our previous tagged analysis [18]. When the two results are combined, we find $y_{CP} = [1.16 \pm 0.22(\text{stat})]\%$, a result with a

![Fig. 1](image-url)
The largest $|\Delta y_{CP}|$ value within each of these two classes of variations is assigned as a systematic uncertainty, 0.0585% for the normalization variations and 0.0624% for the effective lifetime variations, which are then added in quadrature.

We account for a possible bias associated with obtaining the combinatorial lifetime PDF in the lifetime fit mass region from data in the lower and upper mass sidebands by fluctuating the PDF parameters taking into account the correlations and statistical errors resulting from the sideband fits. We construct 100 PDF variations for each of the lower and upper sidebands for each of the final states, and then perform the nominal lifetime fit using each variation. We separately compute

For simulated signal events generated at nominal time.

Additionally find no significant variations in the reconstruction efficiency for signal decays as a function of the true decay time, excluding any systematic uncertainties.

Numerous cross-checks have been performed to assure the unbiased nature of the fit model and to validate the assumptions used in its construction. We have performed fits to datasets composed of fully simulated signal and background events in the proportions seen in the actual data, and find no bias in the measurement of individual $\tau_{K\pi}$ and $\tau_{KK}$ lifetimes for simulated signal events generated at 411.6 fs (very near the nominal $D^0 \rightarrow K^-\pi^+$ lifetime value [18]), or for a lifetime value $\sim$ 10% greater than this for $D^0 \rightarrow K^+K^-$. We additionally find no significant variations in the reconstruction efficiency for signal decays as a function of the true decay time.

Many of the systematic uncertainties associated with the individual lifetime measurements cancel to a great extent in the ratio of lifetimes. We consider as possible sources of systematic uncertainty: variations in the signal and background fit models, changes to the event selection, and detector effects that might introduce biases in the lifetime measurements.

We test the assumption of a shared signal resolution model by separately fitting each mode using completely independent resolution functions, and assign as a systematic uncertainty the magnitude of the change $|\Delta y_{CP}|$ in $y_{CP}$ relative to the result of the nominal fit. We additionally perform the nominal fit using a double Gaussian signal resolution model, and similarly assign a systematic uncertainty. The total uncertainty associated with the choice of signal resolution model is 0.016%.

To estimate possible biases correlated with the extent and position of the lifetime fit mass region, the size of the mass window is varied by $\pm 2$ and $\pm 5$ MeV/$c^2$ without changing the mass region center, and the center is shifted by $\pm 0.5$ MeV/$c^2$ while retaining the nominal 20 MeV/$c^2$ width. The total systematic uncertainty obtained from variations in the lifetime fit mass window is 0.110%.

The modeling of the misreconstructed charm background is taken from simulated events, and we vary the expected contribution from these events by $\pm 15\%$($\pm 5\%$) for the $K^-\pi^+$ ($K^+K^-$) final state. These bounds are conservatively assigned based on the results of other BABAR charm analyses in which the background modes here are fully reconstructed, and in which data and simulated event yields are found to agree within a few percent. We additionally vary the effective lifetime used in the charm background lifetime fit PDFs by the same percentages, which corresponds to $>+2\sigma$ in the statistical uncertainty given the number of simulated events used. The largest $|\Delta y_{CP}|$ value in each of these two classes of variations is assigned as a systematic uncertainty, 0.0585% for the normalization variations and 0.0624% for the effective lifetime variations, which are then added in quadrature.

We account for a possible bias associated with obtaining the combinatorial lifetime PDF in the lifetime fit mass region from data in the lower and upper mass sidebands by fluctuating the PDF parameters taking into account the correlations and statistical errors resulting from the sideband fits. We construct 100 PDF variations for each of the lower and upper sidebands for each of the final states, and then perform the nominal lifetime fit using each variation. We separately compute

![FIG. 2: $D^0 \rightarrow K^-\pi^+$ decay time distribution with the data (points), total lifetime fit (line), combinatorial background (gray) and charm background (black) contributions overlaid.](image1)

![FIG. 3: $D^0 \rightarrow K^+K^-$ decay time distribution with the data (points), total lifetime fit (line), combinatorial background (gray) and charm background (black) contributions overlaid.](image2)
TABLE II: Systematic uncertainties.

| Uncertainty Source                  | $|\Delta y_{CP}|$ (%) |
|-------------------------------------|----------------------|
| Signal resolution model             | 0.016                |
| Mass window                         | 0.110                |
| Misreconstructed Charm model        | 0.086                |
| Combinatorial PDF                   | 0.115                |
| $\sigma_t$ selection                | 0.069                |
| Overlap candidate selection         | 0.017                |
| Detector effects                    | 0.093                |
| **Total**                           | **0.216**            |

the RMS of the 100 $\Delta y_{CP}$ values associated with each of the four sets of variations, and assign the largest RMS, 0.115%, as a systematic uncertainty.

We evaluate systematic uncertainties associated with the selection of the final dataset by individually varying the selection criteria. We change the maximum allowed decay time uncertainty by ±0.1 ps, and assign the largest $|\Delta y_{CP}|$ value, 0.069%, as a systematic uncertainty. We vary the way in which signal candidates that share tracks with other signal candidates are selected by removing all overlapping candidates, and separately by also retaining all such candidates, and again take the larger of the resulting two $|\Delta y_{CP}|$ values, 0.017%, as a systematic uncertainty.

We account for possible detector effects which might bias the lifetime ratio by using several different detector configurations to re-reconstruct simulated event samples with statistics greater than the actual data for each configuration. These configurations include vertex detector misalignments, along with boost and beamspot variations, whose extent is based on residual uncertainties in studies of mu-pair and cosmic events. The misalignment configurations introduce changes of up to 4 fs in both $KK$ and $K\pi$ lifetimes, as well as changes in the offset parameter $t_o$ of up to 5 fs. Since the same simulated event sample is reconstructed for each set of detector configuration, the variations are dominated by systematic effects. The total systematic uncertainty arising from this source is 0.093%.

Table I shows the contribution from each source of systematic uncertainty given above. The total is calculated as the sum in quadrature of each of the individual items. In addition to the contributions quantified in the table, we also look for possible biases by fitting the data separated in: several different data-taking periods; several different azimuthal and polar angle bins in the laboratory frame for the $D^0$ candidate; several bins of the opening angle in the laboratory frame between the two $D^0$ daughters; several bins of the $D^0$ helicity angle; and several bins of the $D^0$ momentum in the CM frame. We observed no significant biases in any of these cases.

In our previously published tagged analysis [18], we combined the tagged result with the result of an untagged BABAR analysis done using a much smaller dataset [21], and this previous untagged result is superseded by the result here, which is $y_{CP}$(untagged) = $1.12 \pm 0.26$ (stat) ±0.22 (syst)% , which excludes the no-mixing hypothesis at 3.3$\sigma$, including both statistical and systematic uncertainties. Our previous tagged result [18] is $y_{CP}$(tagged) = $1.24 \pm 0.39$ (stat) ±0.13 (syst)% . These results contain no events in common, and are thus statistically uncorrelated by construction. However, the degree of correlation in the systematic uncertainties is substantial, and we conservatively assume a 100% correlation in the systematics shared between the two analyses. Combining the tagged and untagged results taking into account both statistical and systematic uncertainties [22], we find $y_{CP}$(correlated) = $1.16 \pm 0.22$ (stat) ±0.18 (syst)% . Summing statistical and systematic uncertainties in quadrature, the significance of this measurement is 4.1$\sigma$.

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