Article

Development and Validation of a Box and Flux Model to Describe Major, Trace and Potentially Toxic Elements (PTEs) in Scottish Soils

Luigi Gallini 1,2,*, Andrew Hursthouse 3 and Antonio Scopa 4,*

Abstract: The box and flux model is a mathematical tool used to describe and forecast the major and trace elements perturbations of the Earth biogeochemical cycles. This mathematical tool describes the biogeochemical cycles, using kinetics of first, second and even third order. The theory and history of the box and flux modeling are shortly revised and discussed within the framework of Jim Lovelock’s Gaia theory. The objectives of the investigation were to evaluate the natural versus anthropic load of Potentially Toxic Elements (PTEs) of the Scottish soils, investigate the soil components adsorbing and retaining the PTEs in non-mobile species, evaluate the aging factor of the anthropic PTEs and develop a model which describes the leaching of PTEs in layered soils. In the Scottish land, the soil-to-rock enrichment factor inversely correlates with the boiling point of the PTEs. The same is observed in NW Italy and USA soils, suggesting the common source of the PTEs. The residence time in soils of the measured PTEs linearly correlates with the Soil Organic Matter (SOM). The element property which mostly explains the adsorption capacity for PTEs’ is the ionic potential (IP). The downward migration rates of the PTEs inversely correlate with SOM, and in Scottish soil, they range from 0.5 to 2.0 cm-year⁻¹. Organic Bentonite is the most important soil phase adsorbing cation bivalent PTEs. The self-remediation time of the polluted soil examined ranged from 50 to 100 years. The aging factor, the adsorption of PTEs’ into non-mobile species, and occlusion into the soil mineral lattice was not effective. The box and flux model developed, tested and validated here does not describe the leaching of PTEs following the typical Gaussian shape distribution of the physical diffusion models. Indeed, the mathematical model proposed is sensitive to the inhomogeneity of the layered soils.

Keywords: soil property variability; soil contamination; pseudo-total elemental pool; box and flux mathematical model

1. Introduction

In the geodynamic earth system, elements cycle between several compartments, most relevant of which are the atmosphere, hydrosphere, pedosphere, biosphere and lithosphere, but also across ecosystems in biogeochemical equilibria with these principal planetary reservoirs. As demonstrated by Jim Lovelock’s Gaia theory, many of the important driving forces of the earth’s dynamic biogeochemical system, as well as most of the relevant geochemical reaction kinetics, rule the flux of elements between the different earth reservoirs, modulated by the biological activity of living organism [1,2]. Most of the
chemical equilibria controlling geodynamics are modulated by simple and multiple retroactive feedback, which ensures some buffering capacity to earth ecosystem and some degree of homeostasis to overall planet earth [3].

Any chemical element is characterized by specific concentration ranges within which the elements may affect organisms living in an ecosystem. The range of Potential Toxic Elements (PTEs) include those with direct toxicity or where they exceed the range of concentration essential or needed for the ecosystem stability and development [4].

Soil as part of the dynamic earth system is the most important planetary sink for many of the PTEs released in the environment by human activity, and since the beginning of the industrial revolution in the 18th Century, there has been an exponential increase in most of the earth environmental ecosystems which are in biogeochemical equilibria, and in particular with soils and sediments.

The intensive agricultural and industrial activity has led to PTE accumulation in agricultural soils threatening the environment, as well as the quality, quantity and security of cultivated products [5]. Many anthropogenic PTEs flushed from contaminated soil into the aquatic ecosystem—and consequently, negatively affecting its biodiversity and stability—eventually accumulate in the marine food chain and affect the security of fish, and the state of human health and fertility rates [6].

The biogeochemical cycles of major chemical elements among earth compartments can be controlled by first-, second-, or even third-order kinetics, but generally the biogeochemical cycles of the PTEs in trace amounts can be described by simple first-order kinetics. The biogeochemical cycles of individual major and trace elements can be coupled together to achieve more detailed and complex models carefully describing the biogeochemical equilibria [7]. It is reasonable to believe that, by coupling together the major element biogeochemical cycles with trace element cycles, we can achieve a more detailed Earth Geochemical Reference Model (GERM). This geochemical reference model could find wide application in the environmental impact assessment of contaminated land and ecosystems (see https://earthref.org/GERMRD/ (accessed on 21 April 2021)).

To evaluate the anthropogenic contribution versus natural origin of the PTEs detected in the environmental compartments, it is critical to estimate the chemical kinetics of the interactions of PTEs with minerals, rocks, solution, gasses and interaction of the bioavailable PTEs with the organism living in the relevant environmental compartment. Fate, mobility, distribution and bioavailability of PTEs depending on the chemical–physical properties of soils, rocks and sediments, which are in turn determined by chemical–physical kinetics reactions mostly controlled by living organisms (these include: complexation, hydrolysis, dissolution, solubility, oxidation, reduction, precipitation, adsorption, methylation and release into atmosphere or translocation, and leaching toward groundwater, uptake into biota, uptake into terrestrial biomass and the related ecosystems) [8]. Most of the rates of the chemical–physical reaction kinetics reported in the literature are enhanced by enzymatic system of living organisms by several orders of magnitude greater than the basic inorganic kinetic reaction rates. As a general rule, the PTEs persist in the earth ecosystem due to the long time required to isolate them in poorly-mobile and non-bioavailable chemical species [9,10].

Box and flux models have been employed to describe the fate and behavior of anthropogenic PTEs fluxes in localized ecosystems. Historically, the box and flux model was initially developed to describe and forecast the leaching of radionuclide in soils [11,12]. With regionalized and georeferenced box and flux models used to describe and forecast the fate and the effects of anthropogenic fluxes of major and trace PTEs in ecosystem Asian oceanic waters [13,14]. The same approach was used to describe and forecast the fluxes of anthropogenic PTEs in the Canadian continental agricultural ecosystem [13,15–19], and employed to describe trace PTEs leaching from soils to groundwater in very localized cases [12,15,20]. Ultimately box and flux models were used to describe and forecast the fluxes of PTEs contaminating pedosphere into the food chain and to evaluate the anthropogenic perturbation of biogeochemical cycles.
Therefore, box and flux models are mathematical tools that are widely used to not only model the earth biogeochemical equilibria, but also the response to perturbation of these equilibria. The box and flux model have been applied to describe the major elements C, N, S and P biogeochemical cycles, but also to evaluate the short- and long-term effects caused by industrial growth that are kinetically perturbing the biogeochemical cycles of the major elements and trace PTEs present in the environmental ecosystem.

In this study, we used local soil systems to determine the soil–rock enrichment factor of PTEs, the anthropogenic PTE load and the properties of the soil that affect the mobility of that pollution. Furthermore, we evaluate the chemical–physical processes and kinetics that remove low-mobile anthropogenic PTEs adsorbed on soil colloids, in insoluble amorphous precipitates and in non-bioavailable phases occluded in the soil, forming crystalline mineral lattices. The ultimate aim of these measures was to develop and validate a new box and flow model that describes the mobility of PTEs in soils and, finally, to determine the so-called “self-remediation” or flushing rates of anthropogenic soil PTEs.

2. Materials and Methods

2.1. Description of Study Area

The soil selected to test and validate the model was developed on the top of a drumlin, several hundred meters long, located in Clelland, South Glasgow, Scotland, UK. The quaternary geology map of the British Geological Survey Service (www.largeimages.bgs.ac.uk/iip/mapsportal.html?id=1003899 (accessed on 21 April 2021)) indicated the soil being studied was derived from a fluvial–glacial parent material that had been deposited during the last glaciations. The alluvial soil was classified as Gleyic Fluvisol [21]. It has been polluted by atmospheric emissions from an adjacent smelter operation, peaking in the 1950s until 1987 when it was decommissioned. Climatic conditions of the area, average of the monthly data, was collected by the Scottish meteorological service (www.metoffice.gov.uk (accessed on 11 June 2000, stored by Gallini L.)), from 1990 to 1995, and are shown in Figure 1.

![Figure 1](image-url)  
Figure 1. Regional climatic data influencing Clelland County, Glasgow, Scotland (UK).

2.2. Soil Profile

Ap horizon (0–25 cm). This was a typically eluvial ploughed horizon, with a sharp boundary and a strong brown color due to the organic matter content. The porosity was high, and the plasticity moderate. The soil aggregates were irregular. Throughout the horizon, strong biological activity was observed: worms and abundant grassroots were found. A relevant flux of PTEs from soil to land biosphere could be expected from Bt horizon due to the intense plants root activity and plants uptake.
Ae horizon (25–35 cm): This was an eluvial horizon below the plough layer. It had a more diffuse boundary with respect to the Ap horizon and a yellow-brown color, which indicates the presence of Goethite and may be the rare mineral forming Maghemite, recognized as an indicator of biomineralization. These iron oxides are shown in the literature to be potential biominerals whose crystallization process is mediated by soil bacterial species. The soil-layer colors and presence of the yellow Goethite indicate a poor drainage state and suggest a seasonal redox oscillation within the Ae horizon, which is confirmed by the estimated soil porosity and the hydrologic balance between precipitation and evapotranspiration (EPT). The Ae horizon had low plasticity and moderate porosity. The soil aggregates were polyhedral with irregular fractures. The cracks observed in the Ae horizon suggest periodic changes in water saturation of the soil and the presence in it of swelling clay minerals in some uncertain amount but below 5%. The biological activity was low and reasonably was mainly represented by soil microflora and soil microfauna.

Bt horizon (35–40 cm). It was an illuvial horizon containing yellowish and greenish lenses that suggested patches of strongly reducing conditions. The red color indicated the presence of iron oxides, such as Hematite, and may be inherited Ilmenite. Porosity and plasticity of the horizon were very high. Soil aggregates were polyhedral with regular fractures, a feature that is proving that swelling clay minerals are present in the Bt horizon in more amount than the upper one Ae. Thin clay films were observed in some polyhedral cracks between aggregates, suggesting that translocation of clay minerals from the upper soil horizon is effective, and they accumulate in the Bt horizon in some quantity. In the Bt horizon, we observed cm diameter stones containing strongly weathered lumps of coal and mixtures of basaltic and sedimentary rock.

2.3. Soil Sampling

Superficial debris and vegetative materials were removed before the collection of samples from the soil surface. The soil was sampled by collecting slices of 5 cm thick at 5 cm increments from a surface of 20 × 20 cm² (about 3 kg dry weight for each layer). Soils were collected in plastic bags, homogenized and air-dried to constant weight, at room temperature; they were then softly disaggregated and sieved to remove coarse debris and rubble (>2.0 mm).

2.4. Analytical Methods

Physical-chemical parameters of soil were determinate in accord with standard methods [22]. The exchangeable pool was determined by extraction of 2 g soil samples (dry weight equivalent) suspended in 20 mL of BaCl₂ (10% w/v at pH = 5.5), so that the precipitation of metal oxides during extraction and the dissolution of any mineral phases were avoided, and were mechanically shaken for 30 min and sonicated for 15 min. The extraction procedure was applied five times until the residue of the extractable pool was negligible. The supernatant was collected by centrifugation and analyzed by ICP–AES or HGA–AAS.

Concentrations of “pseudo-total” metals were determined after digestion of soil samples with aqua-regia, which does not completely destroy silicates [21,23]. Then 2.0 g of dry soil was placed in a digestion vessel with 6 mL of HCl and 14 mL of HNO₃ and digested in microwave digestion unit (MLS-1200 Mega, Milestone Inc., Shelton, CT, USA), at rising temperature steps, and later filtered. The digested samples were analyzed for Si, Al, Fe, Ca, Mg, K, Na, Ni, Co, Cu, Zn, Cr, Mn, P and S by inductively coupled plasma–atomic emission spectrometry (ICP–OES; model iCAP 6000, Thermo-Scientific, Cambridge, UK). A certified standard soil reference material was also analyzed in order to evaluate the method of digestion and the accuracy of analysis (GBW7404). The external standard solutions were derived from 1000 ppm stock metal solution; multi-element standards for calibration were prepared in the same reagents to minimize interferences and matrix effects. Three replicate analyses for samples were performed for all determinations. The Standard
Deviation (SD) was below 10% for pH, texture, Cation Exchange Capacity (CEC), and below 1% for the aqua-regia extractable pool [16,23].

All the chemicals used in this study were analytical grade or better (Sigma-Aldrich, St. Louis, MO, USA) and used without further treatment. Reagent solutions were prepared with deionized water of resistivity not less than 18.2 MΩ·cm⁻¹. The main soil properties are reported in Table 1.

Table 1. Soil properties.

| Depth (cm) | Moisture (%) | Sand (%) | Clay (%) | SOM (%) | CEC Eq/kg | pH | pH | ΔpH |
|-----------|--------------|----------|----------|---------|-----------|----|----|-----|
| 0–5       | 36.6         | 32.7     | 33.60    | 11.59   | 10.83     | 5.10| 4.40| −0.70|
| 5–10      | 32.8         | 10.23    | 20.00    | 7.98    | 9.82      | 4.80| 4.41| −0.39|
| 10–15     | 24.5         | 4.86     | 20.90    | 5.97    | 9.75      | 4.85| 4.42| −0.43|
| 15–20     | 21.3         | 6.74     | 20.00    | 5.00    | 9.77      | 4.88| 4.39| −0.49|
| 20–25     | 21.2         | 5.91     | 24.20    | 5.16    | 8.99      | 4.85| 4.44| −0.41|
| 25–30     | 15.7         | 4.22     | 24.10    | 2.98    | 7.48      | 4.78| 4.39| −0.39|
| 30–35     | 16.6         | 3.47     | 23.00    | 2.15    | 7.03      | 4.76| 4.27| −0.49|
| 35–40     | 21.1         | 2.66     | 31.10    | 1.90    | 8.18      | 4.71| 4.03| −0.68|
| 40–45     | 31.8         | 0.00     | 76.02    | 1.96    | 10.6      | 4.50| 3.71| −0.79|

2.5. Modification of the Bonazzola’s Model

The box and flux model here developed and tested is the generalization of the model of Bonazzola et al. [12]. The main differences of the new box and flux model are the following:

(a) In the top surface reservoirs, a constant atmospheric input I(t) can be considered.
(b) In the model here proposed, each soil reservoir (Sᵢ) is characterized by a specific kinetic constant (Kᵢ) which characterizes any different soil layer—indeed, the averaged K kinetic constant fitted across the entire soil profile, such as the Bonazzola’s box and flux model calculates.
(c) The general solution valid for Sn reservoir is found and proposed—indeed, the only four reservoirs model solution proposed by Bonazzola et al. [12].

As in the Bonazzola’s model, the concentration of the PTEs in the soil profile are subdivided in reservoir “Sn”, and the leaching from a reservoir to the under layer one is assumed to be a first order kinetics. The leaching of the PTEs can be so described by the system of n homogenous differential equations listed below.

$$\frac{dS_0}{dt} = I - F_0 - I - K_0 \times S_0$$

$$\frac{dS_i}{dt} = F_0 - F_1 = (K_0 \times S_0) - (K_1 \times S_1)$$

$$\frac{dS_2}{dt} = F_1 - F_2 = (K_1 \times S_1) - (K_2 \times S_2)$$

$$\frac{dS_3}{dt} = F_2 - F_3 = (K_2 \times S_2) - (K_3 \times S_3)$$

$$\frac{dS_{n-1}}{dt} = F_{n-2} - F_{n-1} = (K_{n-2} \times S_{n-2}) - (K_{n-1} \times S_{n-1})$$

$$\frac{dS_n}{dt} = F_{n-1} - F_n = (K_{n-1} \times S_{n-1}) - (K_n \times S_n)$$

The system is resolvable, and the general solutions are as follows:

1. \[ S_{i,0} = I/K(1) - (I/K(1) \times S_{i,0}) \exp(-K(1) \times t) \]

2. \[ S_{0,0} = I/K(0) + \left[ \sum_{m=1}^{n} (m \rightarrow m = n) (K_{m-1}/K(0) - K(m)) \times A(m-1) \exp(-K(m) \times t) \right] - [I/K(0)S_{0,0} + \sum_{m=1}^{n} (m \rightarrow m = n) (K_{m-1}/K(0) - K(m)) \times A(m-1) \exp(-K(0) \times t)] \]

where
n > 1
\[ A_{(i,1)} = \frac{(S_{i,0} - I/K_i)}{K_i} \]
\[ A_{(n,m)} = [S_{(n,0)} - I/K_{(n)} - \sum(m = 1 \rightarrow m = n)(K_{(n-1)}/(K_{(n)} - K_{(m)}) \times a_{(m,n-1)})\exp(-K_{(m)} \times t)] \]

Three geochemical parameters can be derived from the kinetic constant (Kn) and calculated for each soil reservoir (Sn): (a) residence time of the pollutants in the reservoir Tr; (b) half-life time of the pollutant in the reservoir, t½; and (c) average downward migration rate Vn of the pollutant in the reservoir Sn. The relative formulas are listed as follows:

\[ Tr_n = K_n^{-1} \]
\[ t_{½n} = \ln2 \times K_n^{-1} \]
\[ V_n = K_n \times d_n \]

where \( d_n \) is the thickness of the reservoir Sn.

The residence time (Tr) represents the ratio between the amount of the element in the reservoir and the flux of element throughout the reservoir and at the steady state of the system; the residence time represents the mean time of an element that is remaining in the reservoir.

The half-life time (t½) at the steady state of the system is the time required to remove half of the element pool in the reservoir n. The lower the half-life, the faster the turnover of the element in the reservoir.

The downward migration rate (Vn) represents the average downward migration rate in the reservoir (Sn), and it is related to the partition constant for the adsorbing phases following the equation:

\[ V_n = V_i \times \exp(-\sum i K_{di} \times Q) \]

where \( V_i \) is the downward migration rate in absence of the adsorbing phase, and \( K_{di} \) and \( Q \) are the partition coefficient and the pseudo-total amount of the adsorbing phases “i” respectively pooled in the reservoir Sn. The downward migration rate in absence of adsorbing phases can be assumed to be as follows:

\[ V_0 = (P \times L - EPT)/\theta \]

where P is the rainfall rate, L is the infiltration coefficient, ETP is the sum of EPT and \( \theta \) is the soil porosity.

When the values I(0), S(0,0) and S(n,0) are known the values of the kinetic constant Kn characteristic of the reservoir Sn can be numerically calculated. To calculate Kn from the value of I(0), S(0,0) and S(n,0) the solver extension for Excel was used, and the validity of the solutions found were checked by a self-produced software.

Previous studies have discussed whether the box and flux models applied to forecast the leaching of chemicals in soils are mathematical rather than physical models. Some authors agree that the mathematical box and flux models are predominantly equivalent to the advective–diffusion model at an infinite scale, e.g., when the Sn reservoirs are infinite. A truly physical advective–diffusive model applied to soils requires the determination of several soil properties, such as infiltration rates, soil porosity, pore distribution, soil tortuosity, exchange sites selectivity distribution, colloids surface charge and many other soil properties difficult to be measured, detected or estimated. In this study, a box and flux mathematical model was developed and applied instead of a truly advective–diffusive physical model, as it is more straight forward to develop and numerically solve, and it useful when applied to a layered substrate, such as soil profile [24].

2.6. Hypothesis Applied in the Box and Flux Model and Validation

The history of pollution inputs into the soil is known; the values I(0) and S(0,0) were estimated by the value S(n,0) of the trace elements. Since the beginning of the 1900s until 1987, the soil was ploughed, and therefore the atmospheric input I(0) mostly accumulated
The pedological horizons reflect the soil clay content, which increases sharply in the Ae horizon. There is an increase in Soil Organic Matter in water and assisted by organic colloids from the surface layers. These variations are common in soils with high vertical flushing by soil in clay content is observed in the top layer of the Ap horizon and in the bottom layer of which is homogeneous throughout the three Würm post glacial warm period.

Almost all trace elements were held in the plough layer until the end of ploughing; Trace elements starts to be leached throughout the layers of the soil profile after the end of ploughing; The biological uptake and biological loop of soil-plant-soil transferring fluxes is minimal and can be disregarded at the present time; The atmospheric input \( I_0 \) can be disregarded after the end of smelter activity; With the end of smelter activity the atmospheric input \( I_0 \) can be disregarded after the end of smelter activity; The lithogenic contribution to the trace element pool extracted by aqua-regia can be disregarded, and the \( S_{0,n} \) value of PTEs can be estimated by the aqua-regia extraction at the time of sampling; Most of the trace elements pool was bound to the labile fraction and the ageing factor is reduced. Therefore, the value of \( S_{0,n} \) can be estimated by the aqua-regia extraction at the time of sampling. Anthropogenic PTEs are bound or immobilized in the soil biomass, associated with humic and fulvic compounds, labile soil mineral fraction and biominerals. Anthropogenic PTEs estimated by aqua-regia is almost exhaustive, and only a partially overestimated due to partial dissolution of primary mica by aqua-regia extraction [23,24].

2.7. Statistical Analysis

SPSS statistical package (Window version 25, SPSS Inc., Chicago, IL, USA) was used for data analysis. The analysis of the experimental data was carried out by using one-way ANOVA, Duncan multiple comparison test and Pearson correlation analysis. All significance statements reported in this study are at the \( p < 0.05 \) level [26,27].

3. Results and Discussion

3.1. Soil Profile Properties

The very coarse fraction reflects the sedimentary (primary) features of the parent materials because they are unaffected by pedological processes [28]. The stones are scattered in the Ap horizon, caused by agricultural disturbance, and progressively decrease to zero towards the bottom layer. It is suspected that the parental material was originally sediment in shallow and slow-moving water in fluvial-glacial environment, affected by current activity. A portion of the clay in the Bt horizon is likely to be primary and due to the Würm post glacial warm period. The pedological horizons reflect the soil clay content, which is homogeneous in throughout the three detected horizons. Only a slight increment in clay content is observed in the top layer of the Ap horizon and in the bottom layer of the Ae horizon. These variations are common in soils with high vertical flushing by soil water and assisted by organic colloids from the surface layers. This is a typical condition in a boreal Atlantic strong-weathered soil environment due to the high rainfall rates. The Soil Organic Matter (SOM) content is highest in the Ap horizon and exponentially decreases sharply in the Ae horizon. There is an increase in the organic matter towards the
top of the Ap horizon because of the root zone and degrading organic matter accumulating in the soil canopy. The CEC increases both toward the top and the bottom of the profile. Both organic and inorganic colloids appear to affect the CEC and strong multiple correlations are observed between CEC, SOM and clay content:

\[
\text{CEC} = (0.144 \pm 0.031) \times \text{Clay} + (0.829 \pm 0.185) \times \text{SOM};
\]

\[n = 9, r^2 = 0.948; F = 9.1 \times 10^{-5}\]

The clay and organic matter contribution to CEC can be estimated respectively as 14 and 80 Eq$\cdot$kg$^{-1}$. The clay minerals have a low CEC and poorly crystalline illitic clay minerals are expected to dominate in the soil profile. The amount of exchangeable Na, K, Mg and Ca (Eq$\cdot$kg$^{-1}$) exceeds the CEC; therefore, the soil has an 100% base saturation and is oversaturated with respect to carbonates, condition which theoretically stabilize the formation of pedogenic swelling clay minerals.

The pH ranges from sub-acid to acid and is quite constant along the soil profile. A little increase of the pH is observed in the organic top layer, and a subtle decrement is observed in the clay minerals rich bottom layer of the Bt horizon. The observed pH range is above the pK both of the SOM carboxyl and the clay minerals basal surfaces but is below the pK of Mn, Fe, and Al oxides surfaces. The SOM and the clay minerals are expected to be mostly negatively charged and the oxides are positively charged in the pH range observed in the soil profile. The exchangeable H$^+$ was estimated by pH$_{(KCl)}$ and was constant through the Ap horizon, and increases exponentially below it, in agreement with the observations on the soil colloids, and CEC.

Reducing conditions are evident in the Bt horizon where gray-greenish lens is observed. The relative humidity (RH) can be considered as a broad indication of reducing conditions and correlate with the clay and SOM:

\[
\text{RH}\% = (6.311 \pm 2.943) + (0.277 \pm 0.060) \times \text{Clay} + (1.993 \pm 0.331) \times \text{SOM};
\]

\[n = 9, r^2 = 0.884, F = 1.58 \times 10^{-3}\]

A reducing environmental low oxidative potential is expected to prevail in the bottom of Bt horizon due the high quantity of clay, high relative humidity and low oxygen activity. The pH value is sub-acid for most of the Ap and Ae horizons, but it results in being acid in the Bt, where it is probably buffered by the dissolution and precipitation reactions of oxides.

3.2. Pseudo-Total Elemental Pool

The aqua-regia extracts all the PTEs bound to the soil humic and fulvic compounds, all the PTEs incorporate into soil microfauna and microflora pool, almost all the PTEs bind to soil minerals labile pool, most of the PTEs bound to superior vegetal residues and only a little fraction of the PTEs sinks into primary soil forming minerals. Most of the elements extracted by aqua-regia are therefore the anthropogenic soil PTEs concentration, here mainly due to the smelter plant emission in the atmosphere and its deposition on the top investigated soil layers. The concentration of pseudo-total element pool extracted in the investigated soil reservoirs is reported in Table 2.
It is evident from Table 2 that the PTEs load throughout the examined soil profile is inhomogeneous among the different soil layers, and specific for any element. No element studied shows a Gaussian distribution across the profile, as usually observed in most of the soil analysis published in the literature and observed in the field [23]. It is hypothesized that the PTEs load in any soil layers reflects the adsorbed component in the soil, as well as specific chemical properties of individual PTEs.

When comparing the aqua-regia extracted pool of the trace elements with the averaged soil composition reported in the literature, it is apparent that most of the trace elements in the investigated soil have a concentration close to the global soil average [29,30]. Only in the case of Cd is the soil averaged value exceeded by the aqua-regia’ extract soil-to-crust enrichment factor, which is close to two. It should be noted that the trace metal concentration in the aqua-regia extractable pools and the soil average concentration reported in the literature are not directly comparable, because the global average soil composition quoted in the literature results from a total (HF) digestion and not by aqua-regia extraction. The aqua-regia soil extract and does not allow us to estimate the PTEs occluded in most of the silica primary minerals, and it is believed to be almost everywhere strongly sensitive to anthropogenic soil PTEs load [23,25].

The correlation matrix among the elements of the aqua-regia pool is shown in Table 3, and it allows us to broadly distinguish four groups of the elements with similar distribution in the soil profile. The groups are (a) Na; (b) Al, Fe, Mg, K and Si; (c) Ni, Co, Cu, Zn, Cd, Pb, Mn and Ca; and (d) Cr, P and S.

The concentration of Na has a complex distribution throughout the soil profile and its pseudo-total concentration does not correlate with any other elements. It is reasonable to suppose that the concentration of Na in the soil is affected by the sea aerosol input for the sample site from on-land marine transfer. The concentration of K, Fe, Mg, Al and Si was almost constant within the soil profile, and a concentration peak of these elements are observed in the Bt horizon. Elements K, Mg, Al, Fe and Si results strongly correlate to the clay fraction content, and therefore is reasonable believe that the soil clay minerals are the main source of the aqua-regia extracted pool of these soil chemical element. The group of the bivalent cation elements Ni, Co, Cu, Zn, Cd, Pb, Mn and Ca has complex patterns in the distribution of the concentration along soil profile. Correlations among the concentration of these elements in the soil profile are observed, and correlation varies from weak to strong. The concentrations of the elements of this group are correlated with SOM and for some elements even with the soil clay fraction, such as Ca, Co and Ni. The group of elements stable as anions (Cr, P and S) has a pseudo-total concentration almost monotonically decreasing across the soil profile. Positive strong correlations between pseudo-total pool and organic matter are observed, and it is reasonable to assume that these anionic species are strongly bound to the SOM colloids.

Table 2. Pseudo-total pool concentration (average values).

| Depth (cm) | Al   | Ca   | Fe   | K    | Mg   | Mn   | Na   | P    | Si   | Cd   | Co   | Cu   | Pb   | Zn   |
|------------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| 0–5        | 12,826 | 2050 | 25,701 | 1130 | 1425 | 557  | 30   | 382  | 529  | 289  | 2.03 | 9.22 | 192  | 35   | 34   | 42   | 108  |
| 5–10       | 13,487 | 2135 | 28,916 | 1093 | 1434 | 598  | 12   | 370  | 506  | 266  | 2.63 | 9.50 | 128  | 36   | 30   | 45   | 179  |
| 10–15      | 12,180 | 2395 | 30,045 | 934  | 1415 | 648  | 42   | 377  | 531  | 230  | 1.73 | 11.02 | 98   | 60   | 30   | 42   | 128  |
| 15–20      | 15,142 | 2264 | 29,975 | 1240 | 1583 | 650  | 84   | 391  | 496  | 268  | 1.01 | 11.17 | 98   | 45   | 32   | 40   | 119  |
| 20–25      | 12,384 | 2097 | 29,200 | 981  | 1413 | 685  | 128  | 346  | 460  | 253  | 0.61 | 10.46 | 84   | 33   | 30   | 100  |
| 25–30      | 12,650 | 1747 | 29,104 | 1084 | 1446 | 864  | 100  | 325  | 271  | 260  | 0.25 | 11.42 | 74   | 28   | 27   | 111  |
| 30–35      | 15,402 | 1480 | 29,978 | 1454 | 1908 | 639  | 73   | 280  | 250  | 345  | 1.42 | 8.01  | 71   | 28   | 28   | 154  |
| 35–40      | 14,848 | 1768 | 29,350 | 1343 | 1622 | 722  | 126  | 338  | 323  | 305  | 2.47 | 8.22  | 68   | 46   | 26   | 60   | 63   |
| 40–45      | 23,219 | 2594 | 40,389 | 3760 | 4364 | 454  | 119  | 187  | 187  | 371  | 1.67 | 13.12 | 88   | 37   | 42   | 53   | 71   |
Table 3. Correlation matrix among elements of pseudo-total pool (bold: $p < 0.05$).

|     | Al  | Ca  | Fe  | K   | Mg  | Mn  | Na  | P   | Si  | Cd  | Co  | Cr  | Cu  | Ni  | Pb  | Zn  |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| Al  | 1.00|     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| Ca  | 0.401| 1.00|     |     |     |     |     |     |     |     |     |     |     |     |     |     |
| Fe  | 0.921| 0.536| 1.00|     |     |     |     |     |     |     |     |     |     |     |     |     |
| K   | 0.979| 0.456| 0.936| 1.00|     |     |     |     |     |     |     |     |     |     |     |     |
| Mg  | 0.971| 0.473| 0.952| 0.997| 1.00|     |     |     |     |     |     |     |     |     |     |     |
| Mn  | −0.627| −0.601| −0.507| −0.634| −0.634| 1.00|     |     |     |     |     |     |     |     |     |     |
| Na  | 0.384| −0.079| 0.438| 0.374| 0.371| 0.255| 1.00|     |     |     |     |     |     |     |     |     |
| P   | −0.854| −0.094| −0.854| −0.886| −0.897| 0.372| 0.493| 1.00|     |     |     |     |     |     |     |     |
| Si  | 0.838| −0.090| 0.629| 0.801| 0.783| −0.527| 0.313| −0.837| −0.718| 1.00|     |     |     |     |     |     |
| Cd  | 0.137| 0.120| −0.023| 0.101| 0.070| −0.508| −0.466| 0.077| 0.233| 0.220| 1.00|     |     |     |     |     |
| Co  | 0.462| 0.754| 0.665| 0.541| 0.565| −0.197| 0.253| −0.360| −0.073| −0.019| −0.434| 1.00|     |     |     |     |
| Cr  | −0.227| 0.253| −0.396| −0.168| −0.192| −0.443| −0.701| 0.424| 0.648| 0.164| 0.384| −0.110| 1.00|     |     |     |
| Cu  | 0.075| 0.518| 0.053| −0.097| −0.085| −0.117| −0.135| 0.341| 0.466| 0.370| 0.346| 0.148| −0.015| 1.00|     |     |
| Ni  | 0.759| 0.753| 0.713| 0.812| 0.814| −0.002| −0.531| −0.038| 0.500| 0.117| 0.643| 0.331| 0.034| 1.00|     |     |
| Pb  | 0.561| 0.780| 0.501| 0.568| 0.551| −0.794| −0.229| −0.179| 0.252| 0.267| 0.657| 0.347| 0.390| 0.478| 0.735| 1.00|
| Zn  | −0.410| −0.199| −0.383| −0.449| −0.426| 0.014| −0.763| 0.359| 0.344| −0.297| 0.113| −0.295| 0.224| −0.171| −0.268| −0.200| 1.00|

3.3. Soil Enrichment Factor

The soil to crust enrichment factor is the ratio between the element concentration in the soil and the element concentration in the crust. The soil enrichment factor (SEF) in the investigated soil was calculated by assuming that the pseudo-total pool of the measured elements is due to the anthropic fluxes and to the perturbation of the natural biogeochemical cycles, dividing the aqua-regia extracted pools values for the average crust concentration of the PTEs. The SEF calculated for the soil is reported in Table 4.

Table 4. Soil enrichment factor (SEF) in USA and Clelland (average values).

| Element | SEF USA * | SEF Clelland + | Boiling Point, K |
|---------|-----------|----------------|-----------------|
| Co      | 0.455     | 0.512          | 3200            |
| Ni      | 0.238     | 0.389          | 3186            |
| Cr      | 0.540     | 1.001          | 2945            |
| Cu      | 0.500     | 0.773          | 2840            |
| Mn      | 0.579     | 0.680          | 2235            |
| Pb      | 1.357     | 2.716          | 2022            |
| Ca      | 0.585     | 0.050          | 1757            |
| Zn      | 0.800     | 1.531          | 1180            |
| Cd      | 3.182     | 13.960         | 1040            |
| S       | 6.154     | 1.542          | 718             |
| P       | 0.430     | 0.333          | 550             |

* Bowen [31]; + present investigation.

The enrichment factor for Ca, Mn, Cd, Co, Cr, Cu, Ni, Pb, Zn, P and S in the studied soil result correlates with the USA soil-to-crust enrichment factor.

If the SEF of the S is disregarded, a strong correlation is observed between the pseudo-total SEF in Clelland and the soil enrichment in the USA:

\[
\text{SEF Clelland} = - (1.80 \pm 0.43) + (4.71 \pm 0.35) \times \text{SEF}_{\text{USA}}; \\
\text{n} = 9, r^2 = 0.963, F = 2.83 \times 10^* 
\]

This result is in agreement with previous investigation on anthropic Zn, Pb and Cd in NWItaly [30]. The SEF of Cd, Co, Cr, Cu, Mn, Ni, Pb and Zn observed in the soil does not correlate with the ionic potential (IP) of the element; instead, it negatively correlates
with the boiling temperature of the element (Figure 2). The correlation observed between SEF and element boiling temperature suggests that the SEF of the PTEs is due to the smelter plant activity rather than soil chemical pedological processes both in Clelland, NW Italy, the USA and in Canadian soils [13,15,16,18,31].

![Figure 2. SEF versus boiling point at Clelland.](image)

### 3.4. Residence Time of Element in the Reservoirs

The residence times of the pollutants in the reservoirs of the soil profile are shown in Table 5.

**Table 5. Residence time (years) of PTEs in the soil reservoir (**** = not determinable).**

| Depth (cm) | Na  | Ca  | Co  | Ni  | Cu  | Zn  | Cd  | Pb  | Mn  | Si  | P   | S   |
|------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 0–5        | 6.4 | 16.8| 14.3| 20.0| 14.5| 15.4| 32.3| 66.7| 67.4| 17.1| 22.1| 33.0|
| 5–10       | 1.8 | 8.8 | 7.4 | 8.7 | 7.4 | 15.4| 31.3| 47.6| 36.2| 7.8 | 10.6| 14.8|
| 10–15      | 3.0 | 6.6 | 5.7 | 5.7 | 8.5 | 7.8 | 11.2| 31.3| 26.2| 4.5 | 7.1 | 10.3|
| 15–20      | 3.3 | 4.8 | 4.4 | 4.4 | 5.4 | 5.3 | 4.5 | 20.0| 19.9| 3.8 | 5.6 | 7.2 |
| 20–25      | 3.6 | 6.7 | 3.4 | 3.3 | 3.3 | 3.6 | 2.2 | 13.9| 16.9| 2.8 | 4.0 | 5.3 |
| 25–30      | 2.5 | 2.7 | 3.3 | 2.6 | 2.5 | 3.4 | 1.0 | 2.1 | 19.3| 2.5 | 3.4 | 2.9 |
| 30–35      | 1.8 | 2.3 | 2.3 | 2.7 | 2.3 | 6.0 | 3.3 | 1.5 | 15.3| 3.2 | 3.1 | 2.7 |
| 35–40      | 4.4 | 3.1 | 2.8 | 2.9 | 5.4 | 3.4 | 7.6 | 7.9 | 29.9| 3.6 | 6.8 | 5.4 |
| 40–45      | ****| ****| ****| ****| ****| ****| ****| ****| ****| ****| ****| ****|
| Average    | 3.3 | 6.1 | 5.5 | 6.3 | 6.2 | 7.5 | 11.7| 23.9| 28.9| 5.7 | 7.8 | 10.1|
| SD, %      | 45.3| 73.4| 72.4| 94.0| 65.5| 67.4| 109.5| 97.5| 59.2| 86.7| 79.9| 98.5|

The average residence time (year) is in the following order:

\[
\text{Na}(3.3) < \text{Ca}(4.8) < \text{Co}(5.7) < \text{Ni}(6.3) < \text{Cu}(6.2) < \text{Zn}(7.5) < \text{Pb}(7.8) < \text{S}(10.1) < \text{Cd}(11.7) < \text{Mn}(28.9)
\]

The residence time in the top soil profile is maximum, decreases downward following organic matter distribution and increases again in proximity to the Bt and beyond.

The soil properties which control the residence time have been investigated by forward multiple regression analysis. The main soil property which controls the residence time of Na is the clay content. The main soil property which controls the residence time of the bivalent cations, i.e., Ca, Co, Ni, Cu, Zn, Cd, Pb and Mn, is the SOM, while for the anions (Si, P and S), it is both the organic matter and clay fraction:
The parameter $\alpha$ has been calculated by multiple regression for Ca, Co, Ni, Cu, Zn, Cd, Pb, Mn, Si, P, and S; the results are shown in Table 6, and the slopes of the linear regression results $\alpha$ has been correlated with the IP of the element.

Table 6. Correlation parameter between residence time and organic matter.

| Element | A  | SD% | $r^2$ | F          |
|---------|----|-----|-------|------------|
| Pb      | 5.08 | 10.1 | 0.933 | $6.10 \times 10^{-5}$ |
| Ca      | 1.21 | 7.7  | 0.960 | $1.31 \times 10^{-3}$ |
| Cd      | 2.47 | 17.3 | 0.828 | $1.15 \times 10^{-4}$ |
| Mn      | 1.03 | 11.0 | 0.923 | $5.00 \times 10^{-6}$ |
| Co      | 1.05 | 6.7  | 0.967 | $7.01 \times 10^{-6}$ |
| Zn      | 1.40 | 10.4 | 0.929 | $7.44 \times 10^{-5}$ |
| Ni      | 1.03 | 14.8 | 0.912 | $1.42 \times 10^{-4}$ |
| Cu      | 1.14 | 9.6  | 0.938 | $4.81 \times 10^{-5}$ |
| Si      | 1.13 | 15.1 | 0.914 | $1.52 \times 10^{-4}$ |
| P       | 1.52 | 11.2 | 0.919 | $1.12 \times 10^{-4}$ |
| S       | 2.11 | 11.6 | 0.914 | $1.32 \times 10^{-5}$ |

The results differ between divalent cations and anions. For the divalent cations, the constant $\alpha$ is inversely proportional to the IP of the metal, while, for the anions, it is directly proportional to the IP (Figures 3 and 4).
The regressions observed between parameter $\alpha$ and the IP of the elements are as follows:

Bivalent cations: $\alpha = (7.85 \pm 1.95) - (2.50 \pm 0.80) \times \text{IP} - 1$;
$n = 8, r^2 = 0.622, F = 2.00 \times 10^{-2}$

Anions: $\alpha = (1.88 \pm 0.58) + 0.306 (\pm 0.05) \times \text{IP}$;
$n = 3, r^2 = 0.973, F = 1.05 \times 10^{-1}$

3.5. The Downward Migration Rate of the Pollutants

The calculated downward migration rates are listed in Table 7. The downward migration rates increase in the following order:

$S_{z(0.89)} < Zn_{(0.32)} = P_{(0.92)} = Pb_{(0.93)} < Mn_{(1.06)} < Cu_{(1.14)} < Ca_{(1.21)} \approx Ni_{(1.23)} = Co_{(1.24)} = Si_{(1.26)} < Cd_{(1.42)} < Na_{(1.75)}$
Table 7. Downward migration rates of the pollutants, cm-year⁻¹ (*** = not determinable).

| Sample  | VS | VZn | VR | VPb | V Mn | VCu | VCo | VNi | VZn | VSi | VCd | VNa |
|---------|----|-----|----|-----|------|-----|-----|-----|-----|-----|-----|-----|
| Fapa1.1/9 | 0.16 | 0.33 | 0.23 | 0.08 | 0.37 | 0.35 | 0.30 | 0.25 | 0.35 | 0.29 | 0.16 | 0.79 |
| Fapa1.2/9 | 0.34 | 0.33 | 0.47 | 0.11 | 0.69 | 0.68 | 0.57 | 0.58 | 0.68 | 0.64 | 0.16 | 2.80 |
| Fapa1.3/9 | 0.48 | 0.64 | 0.70 | 0.16 | 0.96 | 0.59 | 0.75 | 0.88 | 0.88 | 1.11 | 0.45 | 1.69 |
| Fapa1.4/9 | 0.69 | 0.94 | 0.90 | 0.25 | 1.25 | 0.93 | 1.04 | 1.13 | 1.14 | 1.32 | 1.12 | 1.52 |
| Fapa1.5/9 | 0.95 | 1.41 | 1.26 | 0.36 | 1.48 | 1.52 | 1.37 | 1.53 | 1.48 | 1.76 | 2.30 | 1.40 |
| Fapa1.6/9 | 1.75 | 1.46 | 1.47 | 2.40 | 1.30 | 2.02 | 1.84 | 1.89 | 1.51 | 2.00 | 5.00 | 1.98 |
| Fapa1.7/9 | 1.85 | 0.83 | 1.62 | 3.45 | 1.63 | 2.14 | 2.23 | 1.85 | 2.14 | 1.54 | 1.51 | 2.72 |
| Fapa1.8/9 | 0.93 | 1.46 | 0.73 | 0.63 | 0.84 | 0.93 | 1.59 | 1.74 | 1.78 | 1.40 | 0.66 | 1.14 |
| Fapa1.9/9 | *** | *** | *** | *** | *** | *** | *** | *** | *** | *** | *** | *** |
| Average | 0.89 | 0.92 | 0.92 | 0.93 | 1.06 | 1.14 | 1.21 | 1.23 | 1.24 | 1.26 | 1.42 | 1.75 |
| SD, % | 69.63 | 51.99 | 52.90 | 137.31 | 40.01 | 58.65 | 54.81 | 50.37 | 47.87 | 44.96 | 114.29 | 40.81 |

As a general rule in the profile, the downward migration rates have a minimum in the top layer, increase to a maximum in the Ae horizon and decrease again approaching the Bt horizon.

It has been assumed that the abundance of the adsorbing phases should be linearly correlated with the logarithm of the downward migration rates, \( V_{(3j)} \) of the element. This has been tested by multiple regression analysis. In Table 8, the correlation matrix between \( \ln(V_e) \) and the soil properties is shown. Most of the PTEs correlate both with SOM and CEC, but the correlation with clay content alone is poor.

Table 8. Correlation between \( \ln(V_e) \) and soil properties (bold: \( p < 0.01 \)).

| \( \ln V_e \) | Moisture | Coarse Fraction | Clay | SOM | CEC | pH | pH |
|-------------|---------|----------------|------|-----|-----|----|----|
| % | % | % | % | Eq/kg | water | KCl |
| \( \ln V_{Co} \) | -0.935 | -0.254 | -0.265 | -0.975 | -0.887 | -0.837 | -0.474 |
| \( \ln V_{Ni} \) | -0.961 | -0.218 | -0.313 | -0.971 | -0.864 | -0.835 | -0.394 |
| \( \ln V_{Cu} \) | -0.894 | -0.122 | -0.343 | -0.822 | -0.898 | -0.682 | -0.145 |
| \( \ln V_{Zn} \) | -0.877 | -0.395 | -0.024 | -0.836 | -0.683 | -0.590 | -0.384 |
| \( \ln V_{Cd} \) | -0.914 | -0.276 | -0.235 | -0.743 | -0.742 | -0.470 | -0.024 |
| \( \ln V_{Pb} \) | -0.882 | -0.440 | -0.094 | -0.848 | -0.977 | -0.647 | -0.376 |
| \( \ln V_{Mn} \) | -0.904 | 0.005 | -0.594 | -0.803 | -0.715 | -0.650 | -0.008 |
| \( \ln V_{Ca} \) | -0.962 | -0.282 | -0.253 | -0.968 | -0.928 | -0.808 | -0.421 |
| \( \ln V_{Na} \) | -0.367 | 0.509 | -0.790 | -0.399 | -0.488 | -0.623 | 0.156 |
| \( \ln V_{Si} \) | -0.954 | -0.121 | -0.431 | -0.909 | -0.771 | -0.769 | -0.211 |
| \( \ln V_{F} \) | -0.954 | -0.111 | -0.481 | -0.865 | -0.834 | -0.704 | -0.100 |
| \( \ln V_{S} \) | -0.971 | -0.260 | -0.303 | -0.938 | -0.937 | -0.770 | -0.315 |

All the soil properties correlated to the \( \ln(V_e) \) have been investigated by using the forward multiple regression method. The meaningful multiple regression funds are listed below.

\[
\ln(V_{Na}) = (2.12 \pm 0.53) - (0.0663 \pm 0.0210) \times \text{Clay}%; \quad n = 8, \quad r^2 = 0.624, \quad F = 1.96 \times 10^{-2}
\]
\[
\ln(V_{Co}) = (1.033 \pm 0.101) - (0.177 \pm 0.016) \times \text{SOM}; \quad n = 8, \quad r^2 = 0.951, \quad F = 3.81 \times 10^{-3}
\]
\[
\ln(V_{Ni}) = (1.164 \pm 0.130) - (0.211 \pm 0.021) \times \text{SOM}; \quad n = 8, \quad r^2 = 0.944, \quad F = 5.69 \times 10^{-3}
\]
\[
\ln(V_{Cu}) = (0.824 \pm 0.278) - (0.160 \pm 0.045) \times \text{SOM}; \quad n = 8, \quad r^2 = 0.676, \quad F = 1.22 \times 10^{-2}
\]
\[
\ln(V_{Zn}) = (0.625 \pm 0.265) - (0.160 \pm 0.043) \times \text{SOM}; \quad n = 8, \quad r^2 = 0.698, \quad F = 9.76 \times 10^{-3}
\]
\[
\ln(V_{Cd}) = (1.259 \pm 0.637) - (0.281 \pm 0.104) \times \text{SOM}; \quad n = 8, \quad r^2 = 0.550, \quad F = 3.48 \times 10^{-2}
\]
\[
\ln(V_{Pb}) = (1.018 \pm 0.571) - (0.365 \pm 0.093) \times \text{SOM}; \quad n = 8, \quad r^2 = 0.720, \quad F = 7.76 \times 10^{-3}
\]
\[
\ln(V_{Mn}) = (0.615 \pm 0.224) - (0.120 \pm 0.036) \times \text{SOM}; \quad n = 8, \quad r^2 = 0.645, \quad F = 1.64 \times 10^{-2}
\]
\[
\ln(V_{Ca}) = (1.093 \pm 0.130) - (0.201 \pm 0.021) \times \text{SOM}; \quad n = 8, \quad r^2 = 0.938, \quad F = 7.73 \times 10^{-5}
\]
\[
\ln(V_{S}) = (0.911 \pm 0.223) - (0.240 \pm 0.036) \times \text{SOM}; \quad n = 8, \quad r^2 = 0.880, \quad F = 5.73 \times 10^{-4}
\]
\[ \ln(V_F) = (0.687 \pm 0.252) - (0.173 \pm 0.041) \times \text{SOM}; \ n = 8, r^2 = 0.748; F = 5.53 \times 10^{-3} \]

The \( \ln(V_{F0}) \) correlates with clay content only. For all bivalent cations and all anions, the \( \ln(V_F) \) the result correlates linearly with SOM (Table 9).

| Element | B   | SD  | C   | SD  | \( r^2 \) | F          |
|---------|-----|-----|-----|-----|----------|------------|
| Pb      | 1.018 |   0.571 | 0.365 | 0.093 | 0.720 | 3.48 \times 10^{-3} |
| Ca      | 1.093 |   0.130 | 0.120 | 0.021 | 0.938 | 7.73 \times 10^{-3} |
| Cd      | 1.259 |   0.637 | 0.281 | 0.104 | 0.698 | 3.48 \times 10^{-2} |
| Mn      | 0.615 |   0.224 | 0.120 | 0.036 | 0.645 | 1.64 \times 10^{-2} |
| Zn      | 0.625 |   0.265 | 0.160 | 0.043 | 0.698 | 9.76 \times 10^{-3} |
| Cu      | 0.824 |   0.278 | 0.160 | 0.045 | 0.676 | 1.22 \times 10^{-2} |
| Ni      | 1.164 |   0.130 | 0.211 | 0.021 | 0.944 | 5.69 \times 10^{-3} |
| Co      | 1.033 |   0.101 | 0.177 | 0.016 | 0.951 | 3.10 \times 10^{-3} |
| S       | 0.911 |   0.223 | 0.240 | 0.036 | 0.880 | 5.70 \times 10^{-4} |
| P       | 0.687 |   0.252 | 0.173 | 0.041 | 0.748 | 5.53 \times 10^{-3} |

Forward multiple regression analysis demonstrates that the bulk clay fraction is not meaningfully correlated to \( \ln(V_F) \) when SOM and clay fraction are considered together. It is reasonable to assume that the downward migration rate of the considered PTEs is sensitive to the mineralogical composition to the clay fraction, as previously demonstrated for \(^{137}\)Cs \([15,31,32]\). Indeed, the Gibbs free energy of the adsorption of cations on clay minerals is very different among the several mineralogical species \([24,33]\).

It has been suggested that the above-reported correlation could be expressed as a linear function of the SOM following the model:

\[ \ln(V_F) = \ln(V_{F0}) - K_{\text{SOM}} \times \text{SOM} \]

Following the proposed linear model, \( \ln(V_{F0}) \) is the logarithm of the downward migration rate in the absence of organic matter, and \( K_{\text{SOM}} \) is the fraction of the mobile element retained in the layer because of the adsorption of the element into the organic matter. The values of \( \ln(V_{F0}) \) and \( K_{\text{SOM}} \) have been estimated by linear regression above.

It is reasonable to assume both the parameters \( \ln(V_{F0}) \) and \( K_{\text{SOM}} \) could be related to chemical properties of the elements.

With respect to anions, no meaningful correlation was found between element properties and \( \ln(V_{F0}) \) or \( K_{\text{SOM}} \). With respect to bivalent cations Co, Ni, Cu, Zn, Mn, Cd, Ca and Pb, the parameter \( \ln(V_{F0}) \) is linearly correlated to the \( \Delta G^* \) of the adsorption of the cation on bentonite for the divalent cations, as shown in the following equation:

\[
\ln(V_{F0}) = (0.689 \pm 0.128) + (0.0123 \pm 0.0047) \times \Delta G^*; \\
n = 6, r^2 = 0.634, F = 5.80 \times 10^{-2}
\]

The downward migration rate \( (V_{F0}) \) of the element therefore decreases exponentially as the adsorption constant on bentonite increases. The parameter \( K_{\text{SOM}} \) for the bivalent cations Co, Ni, Cu, Zn, Mn, Cd, Ca and Pb is resulted inversely proportional to the ionic radius of the element following the linear model:

\[
K_{\text{SOM}} = (0.026 \pm 0.049) + (0.471 \pm 0.121) \times \text{IP} - 1; \\
n = 8, r^2 = 0.671, F = 7.93 \times 10^{-3}
\]

Assuming that the soil properties that control the downward migration rates of the elements do not change with time and are in the steady state, the proposed box and flux model allows us to predict the evolution with time of the element concentration throughout the soil profile. This assumption of the steady state of the soil properties controlling the PTEs leaching is reasonable when the concentration of the SOM pool in the soil profile
has reached the steady state. It is not true if the climate change impact on land biomass and plant productivity are considered.

It is evident from the applied model that the time needed to decreases at half the concentration of the pollutants in the ploughed layer ranges from 25 years for the slowest mobile element (S) to 10 years for the faster moving (Na). The distribution of the pollutant throughout the soil profile calculated by the proposed box and flux model does not follow a Gaussian shape distribution, unlike in the case of the usual convective–advective physical models. It is because some soil reservoirs selectively accumulate some PTEs with respect to others PTEs. The reason for this phenomenon is that the proposed box and flux model is sensitive to the inhomogeneity commonly observed in the layered soil profile.

4. Conclusions

The main pedological processes that are active in the soil profile are ruled by SOM accumulation; weathering of the primary minerals, particularly the mica family; the formation of swelling clay minerals, which are stabilized by the very high soil base saturation; and the translocation and precipitation of soil colloids and oxide phases. The soil profile studied is characterized by almost constant pH values across the profile, which range from acid to slightly-acid. A sharp pH decrease is observed at the top of the Bt horizon, where it is reasonable to suppose it is buffered by iron oxide precipitation. As we observed soil structures and the related colors, wide Eh values are expected because of seasonal weather fluctuations and local soil structures at microscales. Among the elements studied K, Mg, Al and Si extracted by aqua-regia are predominantly derived from illitic minerals, while the aqua-regia extractable pool of Co, Ni, Cu, Zn, Cd, Pb, Mn and Cr is soil contamination derived from the local smelter plant emissions to the atmosphere and deposition on the topsoils. The soil-to-crust enrichment factor of the PTEs is explained by the element boiling point. As the boiling point decreases, the soil-to-rock enrichment factor increases, and with increasing boiling point, the SEF decreases. The same trends were observed in Northern Italy, the USA and in Canadian soils [13,15,16,18,31]. This demonstrates that extensive impact industrial emissions can have on food production. The average downward migration rates range from 0.89 to 1.75 cm\(^{-1}\)y\(^{-1}\), in the following order:

\[
S_{0.89} < Zn_{0.92} = Pb_{0.93} \approx Mn_{1.06} < Cu_{1.14} < Ca_{1.21} = Ni_{1.23} = Co_{1.24} = Si_{1.26} < Cr_{1.37} < Na_{1.75}
\]

The main soil component retarding the leaching of the monovalent Na is the clay fraction. The SOM is not effective in Na adsorption in a detectable way. The main soil component adsorbing the divalent cations and anionic PTEs is the SOM. The SOM and, to the lesser effect, the soil organic Bentonite phase are the main soil components affecting the PTEs mobility. The affinity of the PTEs with the SOM is inversely correlated to the IP. The residence times of the individual PTEs in soil are in the following order:

\[
Na_{1.33} < Ca_{4.8} < Co_{5.5} \approx Si_{5.7} < Ni_{6.2} < Cu_{7.5} < Zn_{7.8} < P_{7.9} < S_{11.1} < Cd_{11.7} < Pb_{23.9} < Mn_{28.9}
\]

The residence time of the Na is ruled by adsorption on clay minerals. The residence time in soils of divalent cations Ca, Co, Ni, Cu, Zn, Cd, Pb and Mn, and the anions Cr, S, Si and P, are ruled by adsorption on SOM. The main PTE property which explains the PTE affinity to the SOM is the IP. The correlations found among the measured PTEs and affinity to soil matter should allow us to estimate the affinity to SOM of PTEs not-measured in our study, such as W, Se, As or the Lanthanides elements for which few data are reported in the literature. The biogeochemical kinetics of the trace PTEs obey first-order kinetics in the box and flux model. The box and flux models proposed and tested here allow us to forecast the downward migration rates and the theoretical time to self-clean polluted soil. The box and flux models describing the leaching in soils of PTEs do not follow the Gaussian distribution shape typical of the physical advective–diffuse models because it is sensitive to layered soil horizon in homogeneity. The result obtained in the Scottish soil agree...
with the data obtained investigating Alpine soils developed on crystalline basement [16,23,34]. The box and flux model has provided a useful geochemical tool to investigate, describe and forecast the fate of trace PTEs contaminating the environmental ecosystems, as well as the potential human health impact of soil contamination by smelter plant activity [13].

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**References**

1. Lovelock, J.E. Gaia as seen through the atmosphere. *Atmos. Environ.* **1972**, *6*, 579–580, doi:10.1016/0004-6981(72)90076-5.
2. Lovelock, J.E.; Margulis, L. Atmospheric homeostasis by and for the biosphere: The Gaia hypothesis. *Tellus* **1974**, *26*, 210, doi:10.1111/j.2153-3490.1974.tb01946.x.
3. Dyke, J.G.; Weaver, I.S. The emergence of environmental homeostasis in complex ecosystems. *PLoS Comput. Biol.* **2013**, *9*, e1003050, doi:10.1371/journal.pcbi.1003050.
4. Pourret, O.; Hursthouse, A.S. It’s Time to Replace the Term “Heavy Metals” with “Potentially Toxic Elements” When Reporting Environmental Research. *Int. J. Environ. Res. Public Health* **2019**, *16*, 4446, doi:10.3390/ijerph16224446.
5. Hu, W.; Wang, H.; Dong, L.; Huang, B.; Borggaard, O.K.; Hansen, H.C.B.; Holm, Y.P.E. Source identification of heavy metals in peri-urban agricultural soils of northeast China: An integrated approach. *Environ. Pollut.* **2018**, *237*, 650–661, doi:10.1016/j.envpol.2018.02.070.
6. Khatri, N.; Tyagi, S. Influences of natural and anthropogenic factors on surface and groundwater quality in rural and urban areas. *Front. Life Sci.* **2015**, *8*, 23–39, doi:10.1007/s11434-014-9337-16.
7. Peng, L.; Liu, P.; Feng, X.; Wang, Z.; Cheng, T.; Liang, Y.; Lin, Z.; Shi, Z. Kinetics of heavy metal adsorption and desorption in soil: Developing a unified model based on chemical speciation. *Geochim. Cosmochim. Acta* **2018**, *224*, 282–300, doi:10.1016/j.gca.2018.01.014.
8. Violante, A.; Cozzolino, V.; Perelomov, L.; Caporale, A.G.; Pigna, M. Mobility and bioavailability of heavy metals and metalloids in soil environments. *J. Soil Sci. Plant Nutr.* **2010**, *10*, 268–292, doi:10.1067/jtsspn.2010.01000005.
9. Charlson, R.J.; Orians, G.H.; Butcher, S.S.; Wolfe, G.V. *Global Biogeochemical Cycles*; Academic Press: Cambridge, MA, USA, 1992.
10. Keller, A.; von Steiger, B.; van der Zee, S.E.A.T.M.; Schulin, R. A stochastic empirical model for regional heavy-metal balances in agro-ecosystems. *J. Environ. Qual.* **2001**, *30*, 1976–1989, doi:10.2134/jeq2001.1976.
11. Poelstra, P.; Frissel, M.J. Migration of water and ions in undisturbed soil columns and its description by simulation models. In *Proceedings of the Symposium on the Use of Isotope and Radiation Techniques in Soil Physics and Irrigation Studies*, Istanbul, Turkey, 12–16 June 1967.
12. Bonazzola, G.C.; Rolopo, R.; Facchinelli, A. Profiles and downward migration of $^{133}$Cs and $^{109}$Ru deposited in Italian soils after Chernobyl accident. *Health Phys.* **1993**, *64*, 479–484, doi:10.1097/00004032-19930500-00004.
13. Sheppard, S.C.; Grant, C.A.; Sheppard, M.J.; de Jong, R.; Long, J. Risk indicator for agricultural inputs of trace elements to Canadian soils. *J. Environ. Qual.* **2009**, *38*, 919–932.
14. Li, K.; Wang, X. Calculation methodology of marine environmental capacity for heavy metal: A case study in Jiaozhou Bay, China. *Chin. Sci. Bull.* **2015**, *58*, 282–287, doi:10.1007/s11434-012-5395-5.
15. Gallini, L.; Facchinelli, A.; Barberis, E.; Ajmone Marsan, F. Cristallochimica e mobilità del radiocesio nei suoli. *Plinius* **1993**, *10*, 157–160.
16. Gallini, L.; Hursthouse, A.; Tucker, P.; Facchinelli, A. An Assessment of the Migration of Heavy Metals in Soils: A Comparison between Central Scotland and NW Italy. In *A Report to British Steel Technology on Work Carried out during September 1997–March 1998*; University of Paisley: Paisley, UK, 1998.
17. Keller, A.; Abbasspour, K.C.; Schulin, R. Assessment of Uncertainty and Risk in Modelling Regional Heavy-Metal Accumulation in Agricultural Soils. *J. Environ. Qual.* **2002**, *31*, 175–187, doi:10.2134/jeq2002.1750.
18. de Vries, W.; Römkens, P.F.A.M.; van Leeuwen, T.; Bronswijk, J.J.B. Heavy Metals. In *Agriculture, Hydrology and Water Quality*, Haygarth, P.M., Jarvis S.C., Eds.; North Wyke Research Station, Institute of Grassland and Environmental Research: Devon, UK, 2002.
19. Semlali, R.M.; Dessogne, J.B.; Monna, F.; Bolte, J.; Azimi, S.; Navarro, N.; Denaix, L.; Loubet, M.; Chateau, C.; van Oort, F. Modelling lead input and output in soils using lead isotopic geochemistry. *Environ. Sci. Technol.* 2004, 38, 1513–1521, doi:10.1021/es0341384.

20. Wang, E.X.; Benoit, G. Fate and transport of contaminant lead in spodosols: A simple box model analysis. *Water Air Soil Pollut.* 1997, 95, 381–397, doi:10.1007/BF02406175.

21. Gallini, L. Inquinamento e Mobilità dei Metalli Pesanti in Prossimità di Uno Stabilimento Siderurgico. Ph.D. Thesis, Università di Torino, Dipartimento di Valorizzazione delle Risorse Agroforestali (Di.Va.P.R.A.), Sezione di Chimica Agraria, Torino, Italy, 2000.

22. Page, A.L.; Miller, R.H.; Keeney, D.R. *Methods of Soil Analysis*; American Society of Agronomy: Madison, WI, USA, 1982; pp. 1–1159.

23. Gallini, L.; Ajmone-Marsan, F.; Scalenghe, R. The contamination legacy of a decommissioned iron smelter in the Italian Alps. *J. Geochem. Explor.* 2018, 186, 121–128, doi:10.1016/j.gexplo.2017.12.013.

24. Bolth, G.H. (Ed.) Soil Chemistry B. In *Physico-Chemical Models*; Elsevier: Amsterdam, The Netherlands, 1979.

25. Riffaldi, R.; Levi-Minzi, R. Il controllo degli inquinanti in agricoltura: Gli inquinanti inorganici. In *Chimica del Suolo*; Sequi, P., Ed.; Patron Editore: Bologna, Italy, 1989; p. 608.

26. Einax, G.W.; Zwanziger, H.W.; Geiß, S. *Chemometrics in Environmental Analysis*; Wiley-VCH: Weinheim, Germany, 2004; p. 403.

27. Miller, J.N.; Miller, J.C. *Statistics and Chemometrics for Analytical Chemistry*, 5th ed.; Pearson Prentice Hall: London, UK, 2005; pp. 1–268.

28. Birkeland, P.W. Soil-geomorphic research—A selective overview. *Geomorphology* 1990, 3, 207–224, doi:10.1016/0169-555X(90)90004-A.

29. Deverel, S.J.; Goldberg, S.R.; Fujii, R. Chemistry of trace elements in soils and groundwater. In *Manual and Reports on Engineering Practice N° 71. ASCE Agricultural Salinity Assessment and Management*, 2nd ed.; Wallender, W.W., Tanji, K.K., Eds.; ASCE American Society of Civil Engineers: Reston, VA, USA, 2012; Chapter 4, pp. 89–137, doi:10.1061/9780784411698.ch04.

30. Facchinelli, A.; Gallini, L.; Barberis, E.; Magnoni, M.; Hursthouse, A.S. The influence of clay mineralogy on the mobility of radiocesium in upland soils of NW Italy. *J. Environ. Radiact.* 2001, 56, 299–307, doi:10.1016/S0265-931X(00)00206-X.

31. Bowen, H.J.M. *Environmental Chemistry of the Elements*; Academic Press: London, UK, 1979; pp. 32–46.

32. Facchinelli, A.; Gallini, L.; Barberis, E.; Hursthouse, A.S. Factor controlling the mobility of radiocesium in soils.1-Soil properties and mineralogy. *Fresenius Environ. Bull.* 1995, 4, 701–705.

33. Facchinelli, A.; Sacchi, E.; Mallen, L. Multivariate statistical and GIS-based approach to identify heavy metal sources in soils. *Environ. Pollut.* 2001, 114, 313–324.

34. Gupta, S.S.; Bhattacharyya, K.G. Adsorption of heavy metals on kaolinite and montmorillonite: A review. *Phys. Chem. Chem. Phys.* 2012, 14, 6698–6723.