Binary Stars Can Provide the “Missing Photons” Needed for Reionization

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ABSTRACT
Empirical constraints on reionization require galactic ionizing photon escape fractions \( f_{\text{esc}} \gtrsim 20\% \), but recent high-resolution radiation-hydrodynamic calculations have consistently found much lower values \( \sim 1\text{–}5\% \). While these models include strong stellar feedback and additional processes such as runaway stars, they almost exclusively consider stellar evolution models based on single (isolated) stars, despite the fact that most massive stars are in binaries. We revisit these calculations, combining radiative transfer and high-resolution cosmological simulations from the FIRE project. For the first time, we use a stellar evolution model that includes a physically and observationally motivated treatment of binaries (the BPASS model). Binary mass transfer and mergers enhance the population of massive stars at late times \( \gtrsim 3\text{Myr} \) after star formation, which in turn strongly enhances the late-time ionizing photon production (especially at low metallicities). These photons are produced after feedback from massive stars has carved escape channels in the ISM, and so efficiently leak out of galaxies. As a result, the time-averaged “effective” escape fraction (ratio of escaped ionizing photons to observed 1500Å photons) increases by factors \( \sim 4\text{–}10 \), sufficient to explain reionization. While important uncertainties remain, we conclude that binary evolution may be critical for understanding the ionization of the Universe.

Key words: binaries: general – stars: evolution – galaxies: formation – galaxies: high-redshift – cosmology: theory

1 INTRODUCTION

The escape fraction \( f_{\text{esc}} \) of hydrogen ionizing photons from high-redshift star-forming galaxies is perhaps the most important and yet most poorly understood parameter in understanding the reionization history. Models of cosmic reionization suggest that \( f_{\text{esc}} \gtrsim 20\% \) (e.g. Kuhlen & Faucher-Giguère 2012; Pikel’stein et al. 2012; Robertson et al. 2013, 2015) is needed to match the optical depth of electron scattering inferred from cosmic microwave background (CMB) measurements (e.g. Hinshaw et al. 2013; Planck Collaboration 2015), assuming that most of the ionizing photons come from star-forming galaxies brighter than \( M_{\text{UV}} = -13 \).

However, such a high \( f_{\text{esc}} \) is problematic in the context of both observations and theory. From the local universe to redshift \( z \sim 1 \), there is no confirmed Lyman continuum (LyC) detection, neither from individual galaxies nor from stacked samples, implying upper limits of \( f_{\text{esc}} = 1\text{–}3\% \) (e.g. Leitet et al. 2011, 2013; Bridge et al. 2010; Siana et al. 2010). Even at \( z \sim 3 \), many earlier reports of LyC detection from Lyman break galaxies (LBGs) and Ly\( \alpha \) emitters (LAEs) have proven to be contaminated by foreground sources (e.g. Siana et al. 2011) and a low \( f_{\text{esc}} \) about 5% has been derived from some galaxy samples at this redshift (e.g. Iwata et al. 2009; Boutsia et al. 2011).

Moreover, the latest generation of cosmological hydrodynamic simulations predict \( f_{\text{esc}} \) to be no more than a few percent in galaxies more massive than \( 10^{9} M_\odot \) in halo mass at \( z > 6 \) (e.g. Wise et al. 2014; Kimm & Cen 2014; Paardekooper, Khochfar & Dalla Vecchia 2015; Ma et al. 2015). These simulations include detailed models of ISM physics, star formation, and stellar feedback, in contrast to early generations of simulations which tended to over-predict \( f_{\text{esc}} \) by an order of magnitude, owing to more sim-
plastic ISM models (see Ma et al. 2015 and references therein). The low $f_{\text{esc}}$ in these simulations is due to the fact that newly formed stars, which dominate the intrinsic ionizing photon budget, begin life buried in their birth clouds, which absorb most of the ionizing photons. By the time low column density escape channels are cleared in the ISM, the massive stars have begun to die and the predicted ionizing photon luminosity has dropped exponentially. Stellar populations older than 3 Myr have order unity photon escape fractions, but – according to single stellar evolution models such as STARBURST99 (Leitherer et al. 1999) – these stars only contribute a small fraction of the intrinsic ionizing photon budget (Ma et al. 2015).

Therefore, there appears to be a factor of $\sim 4$–5 fewer ionizing photons predicted, compared to what is needed to ionize the Universe. Several solutions have been proposed. For example, Wise et al. (2014) suggested that tiny galaxies that are much fainter than $M_{\text{UV}} = -13$ may play a significant role in reionization, since $f_{\text{esc}}$ increases quickly from 5% to order unity for halo mass below $10^{10.5} M_\odot$. However, others have noted that the required number of tiny galaxies would imply a huge population of Milky Way satellites which have not been observed (see Boylan-Kolchin, Bullock & Garrison-Kimmel 2014; Graus et al. 2016). Conroy & Kratter (2012) proposed that runaway OB stars can boost $f_{\text{esc}}$; however both Kimm & Cen (2014) and Ma et al. (2015) showed that in high-resolution simulations these produce a marginal effect, increasing $f_{\text{esc}}$ systematically by a factor of only $\sim 1.2$ (far short of the $\gtrsim 4$ required). A more radical alternative is to invoke non-stellar sources for reionization, for example AGN (see e.g. Madau & Haardt 2015). This relies on recent observations (e.g. Giavalisco et al. 2015) that show that the time-averaged $f_{\text{esc}}$ is about 5% for galaxies of halo masses from $10^{9}$–$10^{11} M_\odot$ at $z = 6$ using the single-star evolution models from STARBURST99. Importantly, we showed that the results were robust to the resolution of both the radiative transfer calculation and the hydrodynamics (once sufficient resolution for convergence was reached), to variations of the star formation and stellar feedback model, and even to the inclusion of large populations of runaway stars. We will show here, however, that the inclusion of binary evolution effects increases the predicted escape fractions substantially, reconciling them with constraints on reionization. We describe the simulation and radiative transfer code in Section 2 present the results in Section 3 and conclude in Section 4.

We adopt a standard flat $\Lambda$CDM cosmology with cosmological parameters $H_0 = 70.2$ km s$^{-1}$ Mpc$^{-1}$, $\Omega_m = 0.728$, $\Omega_{\Lambda} = 1 - \Omega_m = 0.272$, $\Omega_b = 0.0455$, $\sigma_8 = 0.807$ and $n = 0.961$, consistent with observations (e.g. Hinshaw et al. 2013; Planck Collaboration et al. 2014).

## 2 METHOD

In this work, we study the effect of binary evolution on $f_{\text{esc}}$ using three galaxies from a suite of cosmological zoom-in simulations presented in Ma et al. (2015). The simulation and radiative transfer are identical. We only replace the stellar evolution model used for the post-processing radiative transfer calculations. This is likely to result in a lower limit on the impact of binaries on $f_{\text{esc}}$, because we do not include the enhanced radiative feedback due to binaries in our simulation. We briefly review the methodology here, but refer to Ma et al. (2015) for more details.

The simulations are part of the Feedback in Realistic Environment project (FIRE; Hopkins et al. 2014). They are run using GIZMO (Hopkins 2015) in P-SPH mode, which adopts a Lagrangian pressure-entropy formulation of the smoothed particle hy-

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### Table 1. Simulations analyzed in this paper.

| Name        | $m_b$ (M⊙) | $\epsilon_b$ (pc) | $m_{\text{min}}$ (M⊙) | $M_{\text{UV}}$ (M⊙) | $M_*$ (M⊙) | $M_{\text{UV}}$ (AB mag) |
|-------------|------------|-------------------|------------------------|-----------------------|------------|--------------------------|
| z5m09       | 16.8       | 0.14              | 81.9                   | 5.6                   | 7.6e8      | 3.1e5                    | -10.1        |
| z5m10mr     | 1.1e3      | 1.9               | 5.2e3                  | 14                    | 1.5e10     | 5.0e7                    | -17.5        |
| z5m11       | 2.1e3      | 4.2               | 1.0e4                  | 14                    | 5.6e10     | 2.0e8                    | -18.5        |

### Notes.
- Initial conditions and galaxy properties at $z = 6$.
- (1) Name: Simulation designation.
- (2) $m_b$: Initial baryonic particle mass.
- (3) $\epsilon_b$: Minimum baryonic force softening. Force softening is adaptive.
- (4) $m_{\text{min}}$: Dark matter particle mass in the high-resolution regions.
- (5) $\epsilon_{\text{dm}}$: Minimum dark matter force softening.
- (6) $M_{\text{UV}}$: Halo mass of the primary galaxy at $z = 6$.
- (7) $M_*$: Stellar mass of the primary galaxy at $z = 6$.
- (8) $M_{\text{UV}}$: Galaxy UV magnitude (absolute AB magnitude at 1500 Å).
dynamics (SPH) equations that improves the treatment of fluid-mixing instabilities (Hopkins 2013). Galaxy properties at $z = 6$ for the three simulations used in this work ($z_{609}$, $z_{610}$, and $z_{611}$) are listed in Table 1. Our simulations span halo masses from $10^7$ to $10^{14} M_{\odot}$ at $z = 6$. These galaxies lie on the low-mass extrapolations of the observed stellar mass–halo mass relation and SFR–stellar mass relation at $z > 6$ (Ma et al. 2015). At lower redshifts (where observations exist at these masses), the simulations have been reproduced to observed scaling relations and chemical abundances (Hopkins et al. 2014; Ma et al. 2016), properties of galactic outflows and circum-galactic absorbers (Muratov et al. 2015; Faucher-Giguère et al. 2015, 2016), and abundances and kinematics of observed (local) dwarfs in this mass range (Onorbe et al. 2015; Chan et al. 2015).

In the simulations, gas follows an ionized–atomic–molecular cooling curve from $10^{-10}$ K, including metallicity-dependent fine-structure and molecular cooling at low temperatures and high-temperature metal-line cooling for 11 separately tracked species (Wiersma, Schaye & Smith 2009). We do not include a primordial chemical network nor consider Pop III star formation, but apply a metallicity floor of $Z = 10^{-4} Z_{\odot}$. At each timestep, the ionization states are determined following Katz, Weinberg & Hernquist (1996) and cooling rates are computed from a compilation of CLOUDY runs, including a uniform but redshift-dependent photo-ionizing background tabulated in Faucher-Giguère et al. (2009), and an approximate model of photo-ionizing and photo-electric heating from local sources. Gas self-shielding is accounted for with a local Jeans-length approximation, which is consistent with the radiative transfer calculations in Faucher-Giguère et al. (2010). The on-the-fly calculation of ionization states is consistent with more accurate post-processing radiative transfer calculations (Ma et al. 2015).

We follow the star formation criteria in Hopkins, Narayanan & Murray (2013) and allow star formation to take place only in dense, molecular, and self-gravitating regions with hydrogen number density above a threshold $n_{\text{H}} = 50$ cm$^{-3}$. Stars form at 100% efficiency per free-fall time when the gas meets these criteria, and there is no star formation elsewhere. Because we require star-forming gas to be self-gravitating, its effective density is even higher than the fiducial density threshold we adopt in our simulations. We emphasize the importance of resolving the formation and destruction of individual star-forming regions in accurately predicting $f_{\text{esc}}$, as stressed also in other studies (e.g. Kimm & Cen 2014; Paardekooper, Kehoe & Dalla Vecchia 2015; Ma et al. 2015). Simulations using unphysically low $n_{\text{H}}$ fail to resolve this and tend to over-predict $f_{\text{esc}}$ by an order of magnitude (see Ma et al. 2015 and reference therein).

The simulations include several different stellar feedback mechanisms, including (1) local and long-range momentum flux from radiative pressure, (2) energy, momentum, mass and metal injection from SNe and stellar winds, and (3) photo-ionization and photo-electric heating. We follow Wiersma et al. (2009) and include metal production from Type-II SNe, Type-Ia SNe, and stellar winds. Every star particle is treated as a single stellar population with known mass, age, and metallicity, assuming a Kroupa (2002) initial mass function (IMF) from $0.1-100 M_{\odot}$. The feedback strengths are directly tabulated from STARBURST99.

For each snapshot, we map the main galaxy onto a Cartesian grid of side length $L$ equal to two virial radii and with $N$ cells along each dimension. We choose $N = 256$ for $z_{609}$ and $z_{610}$ and $N = 300$ for $z_{611}$, so that the cell size $l = L/N$ varies but is always smaller than 100 pc. This ensures convergence of the MCRT calculation (Ma et al. 2015). The MCRT code we use is derived from the MCRT code SEDONA (Kasen, Thomas & Nugent 2006), but focuses on radiative transfer of hydrogen ionizing photons. The MCRT method is similar to that described in Hunagali et al. (2011, 2014), $N_{\text{MCRT}} = 3 \times 10^7$ photon packets are isotropically emitted from the location of star particles, sampling their ionizing photon budget. Another $N_{\text{UVB}} = 3 \times 10^7$ photon packets are emitted from the boundary of the computational domain in a manner that produces a uniform, isotropic ionizing background with intensity given by Faucher-Giguère et al. (2009). The MCRT code includes photoionization, collisional ionization, recombination, and dust absorption and uses an iterative method to reach photoionization equilibrium. The numbers of photon packets and iteration are selected to ensure convergence.

3 RESULTS

We use $Q_{\text{ion}}(t)$ to represent the ionizing photon production rate (number of ionizing photons produced per second) and

$$Q_{\text{ion}}(> t) = \int_{t}^{\infty} Q_{\text{ion}}(t') \, dt'$$

(1)

to represent the number of ionizing photons produced after time $t$. In Figure 1, we show $Q_{\text{ion}}(t)$ (upper panel), the fraction of ionizing photons emitted after time $t$, $Q_{\text{ion}}(> t)/Q_{\text{ion}}(> 0)$ (middle panel), and the ratio between ionizing luminosity and the luminosity at 1500 Å,

$$\xi_{\text{ion}} = \frac{\int_{\lambda_{1500}}^{911 \text{ Å}} L_{\lambda} \, d\lambda}{\lambda L_{\lambda}(1500 \text{ Å})}$$

(2)

(bottom panel), as a function of age, of an instantaneously formed star cluster of mass $10^9 M_{\odot}$, for several stellar population models from BPASS. We adopt a Kroupa (2002) IMF with slopes of $-1.3$ from 0.1–0.5 $M_{\odot}$ and $-2.35$ from 0.5–100 $M_{\odot}$, consistent with that used in the simulation. We show the BPASS model at metallicity $Z = 0.001$ ($Z = 0.05 Z_{\odot}$, black), the lowest metallicity available and the closest to our simulations, for both single-star evolution (dotted) and binary evolution (solid) models. We also compare those with $Z = 0.02$ ($Z = Z_{\odot}$, cyan) models from BPASS. We note that the STARBURST99 models (not shown), which are the default model in Ma et al. (2015), are nearly identical to the single-star model from BPASS at both metallicities.

The ionizing photon production rates in the single-star and binary models are very similar for the first 3 Myr, but start to differ significantly after 3 Myr at $Z = 0.05 Z_{\odot}$, with the binary model producing an order of magnitude more ionizing photons by 10 Myr. Also, in the binary model, the production of ionizing photons is more extended. For example, almost 60% (20%) of the ionizing photons are produced after 3 Myr (10 Myr), while this fraction is 40% (1%) in single-star model. These late-time photons can escape more easily so one should expect them to make a big difference on $f_{\text{esc}}$ (as confirmed by MCRT calculations below). However, at solar metallicity, these fractions are much lower and the difference between single-star and binary models is less significant.

To illustrate the effects of binaries, we run our MCRT code on the main galaxy in our $z_{610}$ simulation ($a = 10^{10} M_{\odot}$ halo at $z = 6$) and compute $f_{\text{esc}}$ using both single-star and binary BPASS models with $Z = 0.05 Z_{\odot}$. The results are presented in Figure 2. Lines and symbols show the instantaneous value and time-averaged values over $\sim 100$ Myr, respectively. Dotted lines and open symbols represent the single-star model, while solid lines and filled symbols
represent the binary model. From top to bottom, the three panels show $f_{\text{esc}}$ (the “true” fraction of ionizing photons that escape the galaxy virial radius), $\xi_{\text{ion}}$, and the “effective” escape fraction from $z = 5.5$–8. The effective escape fraction is defined as

$$f_{\text{esc, eff}} = f_{\text{esc}} \frac{\xi_{\text{ion}}}{\langle \xi_{\text{ion}} \rangle_{\text{single}}} ,$$

which is the ratio of the escaping ionizing flux to 1500 Å flux, relative to what would be computed using single-star models. $f_{\text{esc, eff}}$ simply equals $f_{\text{esc}}$ for single-star models, while for binary models, it also accounts for the change of $\xi_{\text{ion}}$ relative to single-star models.

The instantaneous $f_{\text{esc}}$ is highly time-variable, associated with stochastic formation and destruction of individual star-forming clouds (consistent with several other studies [Wise et al. 2014, Kimm & Cen 2014, Paardekooper, Khochfar & Dalla Vecchia 2015]). For single-star models, $f_{\text{esc}}$ is below 5% most of the time, because young stars are buried in their birth clouds, which prevent almost all ionizing photons from escaping. Most of the photons that escape come from stellar populations with age $\sim 3$–10 Myr, but they only contribute a very small fraction of the intrinsic ionizing photons in single-star models (Ma et al. 2015). However, at all times, the binary model predicts significantly higher (factors $\sim 3$–6) values for $f_{\text{esc}}$. We also find that $\xi_{\text{ion}}$ is boosted by a factor of
stellar evolution models ignoring binaries. These later-time photons easily escape, collectively increasing the escape fraction and ionizing photon production rate dramatically from high-redshift low-metallicity galaxies.

For single-star evolution models, we predict $f_{esc}$ below 5% most of the time, less than what is required ($\sim 20\%$) for cosmic reionization. However, when accounting for binary effects, $f_{esc}$ can be boosted by factors of $\sim 3-6$ and $\xi_{\text{esc}}$ can be boosted by a factor of 1.5. Therefore, the "effective" escape fraction (the ratio of escaped ionizing photon flux to 1500 Å flux) can be boosted by factors of $\sim 4-10$. For the more massive galaxies in our simulation, this brings them into good agreement with the values required to ionize the Universe.

We emphasize that the most important change relative to single-star models is not in the absolute photon production rate, but its time-dependence, because photons emitted after 3 Myr can much more easily escape star-forming complexes once feedback from massive stars has destroyed the dense birth cloud. Moreover, we have exhaustively tested in a previous study (Ma et al. 2015) that these results are not sensitive to our star formation and stellar feedback models. For example, increasing the strength of all feedback (radiation, stellar winds, SNe) per star particle relative to our fiducial model simply leads to self-regulation at lower star formation rates, giving an identical prediction for $f_{esc}$. Likewise, increasing the density threshold for star formation, re-distributing ionizing photons to fewer but more luminous particles, increasing the ionizing photon production rate used for feedback in the code, all produce similar predictions for $f_{esc}$.

Nevertheless, the binary fraction in high-redshift galaxies and the details of binary evolution are both uncertain, so our results are not definitive. They do, however, demonstrate the potential for binary evolution to reconcile empirical constraints on reionization by starlight with observations and simulations. In principle, these models can be confronted by the observed GRB rates at these redshifts (e.g. Kistler et al. 2009; Wyithe et al. 2010), although large uncertainties remain. In addition, the BPASS model does not include stellar rotation before binary interaction, which may also significantly increase the intrinsic ionizing photon production rate (e.g. Topping & Shull 2015). Rotation likely has a smaller effect on $f_{esc}$ because most of the extra ionizing photons it predicts are produced less than 3 Myr after star formation.

We have repeated our radiative transfer calculation on cosmological simulations of Milky Way-mass galaxies at $z = 0$ ($Z \sim Z_\odot$) from the FIRE project (see Hopkins et al. 2014 for details). We find that binaries appear to be enhancing $f_{esc}$ by only a factor $\sim 1.5$ at solar metallicity. This is expected since binary effects tend to be weaker at higher metallicities (also see Figure 1), for at least three reasons: (1) the number of ionizing photons decreases significantly as stellar atmospheres are cooler, (2) quasi-homogenous evolution ceases to apply above $Z = 0.004 \ (Z = 0.2 \ Z_\odot)$, and (3) stellar winds become stronger, reducing the lifetime of massive stars and suppressing the mass transferred between binaries. In addition, the absolute time-averaged $f_{esc}$ does not exceed $\sim 3\%$ in these galaxies, consistent with observational constraints in the local Universe (see references in Section 1). It appears that these galaxies are forming stars in a more "calm", less-bursty mode compared to the high-redshift dwarfs here (e.g. Sparre et al. 2015), and maintain much larger reservoirs of neutral gas in their galactic disks, which leads to much larger absorption even of photons produced by intermediate-age massive stars. A detailed study will be presented in a separate paper (Su et al., in preparation).

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure3}
\caption{Effective escape fraction as a function time for $z5m09$ and $z5m11$. Like $z5m10$ (Figure 2), binary stellar models boost $f_{\text{esc,eff}}$ by factors of $\sim 4-10$. In more massive galaxies, the mean $f_{\text{esc,eff}}$ reaches $\sim 20\%$, sufficient for reionization.}
\end{figure}

4 DISCUSSION AND CONCLUSIONS

In this work, we study the effect of binary evolution on ionizing photon production and escape in high-redshift galaxies, using three high-resolution cosmological simulations from the FIRE project. The simulated galaxies are around the mass estimated to dominate re-ionization ($M_{\text{halo}} = 10^9-10^{11} M_\odot$ at $z = 6$). Using detailed radiative transfer calculations, we show that recent stellar evolution models which account for mass transfer and mergers in binaries (specifically, the BPASS model) produce significantly more ionizing photons for stellar populations older than 3 Myr compared to
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