Stanene-hexagonal boron nitride heterobilayer: Structure and characterization of electronic property

Asir Intisar Khan, Trisha Chakraborty, Niloy Acharjee & Samia Subrina

The structural and electronic properties of stanene/hexagonal boron nitride (Sn/h-BN) heterobilayer with different stacking patterns are studied using first principle calculations within the framework of density functional theory. The electronic band structure of different stacking patterns shows a direct band gap of ~30 meV at Dirac point and at the Fermi energy level with a Fermi velocity of ~0.53 × 10^6 ms^-1. Linear Dirac dispersion relation is nearly preserved and the calculated small effective mass in the order of 0.05m indicates high carrier mobility. Density of states and space charge distribution of the considered heterobilayer structure near the conduction and the valence bands show unsaturated π orbitals of stanene. This indicates that electronic carriers are expected to transport only through the stanene layer, thereby leaving the h-BN layer to be a good choice as a substrate for the heterostructure. We have also explored the modulation of the obtained band gap by changing the interlayer spacing between h-BN and Sn layer and by applying tensile biaxial strain to the heterostructure. A small increase in the band gap is observed with the increasing percentage of strain. Our results suggest that, Sn/h-BN heterostructure can be a potential candidate for Sn-based nanoelectronics and spintronic applications.

Of late, group-IV two dimensional (2D) materials such as silicene, germanene and stanene have received special attention attributed to their similar electronic properties with the graphene and intriguing prospects in the nanoelectronic device applications. In fact, stanene, a buckled honeycomb structure of 2D hexagonal tin film, has drawn keen interest due to its intriguing prospect as quantum Hall insulator, topological insulator and topological superconductor. In addition, stable low buckled form of stanene, synthesized on the Bi₂Te₃ (111) substrate is theoretically investigated to support a large-gap 2D quantum spin Hall (QSH) state at room temperature and enables superior electric conduction with zero dissipation. However, stanene has a zero band gap without spin orbiting coupling (SOC) while ~0.1 eV SOC induced band gap has been reported in the literature. This zero band gap feature limits the use of stanene in the high performance semiconductor based nanoelectronic devices such as field effect transistor. In this context, Garg et al. has recently reported the opening of a band gap in stanene by the patterned boron-nitride (BN) doping in stanene using density functional theory (DFT). In addition, Chen et al. has studied graphene-stanene heterobilayer models with several stacking methods and reported a band gap of ~77 meV for the most stable configuration. Furthermore, graphene/hexagonal boron nitride (graphene/h-BN) bilayer has been reported to show a small band gap at Dirac point in contrast to the zero band gap of graphene monolayer as well as higher carrier mobility than the graphene bilayers. In fact, chemical stability and significant band gap of the monolayer h-BN make it promising for heterostructure based nano-devices.

Hence, following the deep scientific interest in modulating the band gap and other electronic properties while preserving the Dirac cone of stanene, we report the structural and electronic properties of stanene/hexagonal boron nitride (Sn/h-BN) heterobilayer using first-principles density functional theory (DFT) calculations. A band gap opening along with the appearance of nearly linear relation near the Dirac point is observed in the proposed heterobilayer structure. Three representative models of the hybrid structure based on different stacking

Department of Electrical and Electronic Engineering, Bangladesh University of Engineering and Technology (BUET), Dhaka, 1205, Bangladesh. Trisha Chakraborty and Niloy Acharjee contributed equally to this work. Correspondence and requests for materials should be addressed to S.S. (email: samiasubrina@eee.buet.ac.bd)
are investigated in terms of their stability, electronic property such as band structure, density of states, real space charge density and effective mass as well as the modulation of band gap under tensile strain and varying the interlayer distance. Our proposed structures with a finite band gap and high carrier mobility would provide further insight and encouragement on the modeling of stanene-based nanoelectronic and spintronic devices.

**Methods**

The electronic properties of the proposed heterobilayer structure are investigated using the density functional theory (DFT) with a plane-wave basis set using the Ab initio code PWSCF package of Quantum Espresso. The electron-ion interactions are accounted using norm conserving Troullier Martin pseudo-potentials. To describe the electron exchange correlation energy, the generalized gradient approximation (GGA) with Perdew-Burke-Ernzerhof (PBE) exchange correlation functional is implemented. In order to consider the Van der Waals (vdW) inter-molecular attractive forces, we have used DFT-D2, an empirical dispersion correction proposed by Grimme throughout the simulations. For the structural optimization, the plane wave basis cut off is set at 550 eV (40 Ry) with a convergence threshold on force of $10^{-4}$ Ry/a.u. The first Brillouin zone of the unit cell is sampled with a $12 \times 12 \times 1$ Monkhorst-Pack grid for the geometry optimization and a $15 \times 15 \times 1$ grid for the subsequent calculations. The interaction between the two adjacent bilayers is eliminated by introducing a sufficient vacuum of 20 Å along the direction perpendicular to the surface.

The effective masses of electrons ($m^*$) and holes ($m_h^*$) have been calculated from the curvature of the conduction band minimum and the valence band maximum respectively at the Dirac point for the three (3) configurations of stanene/h-BN heterobilayer using the following formula:

$$m^* = \hbar^2 \left( \frac{\partial^2 E(k)}{\partial k^2} \right)^{-1}$$  \hspace{1cm} (1)

where, $m^*$ is the particle effective mass, $E(k)$ is the dispersion relation, $k$ is the wave vector and $\hbar$ is the reduced Planck constant.

**Results and Discussions**

In our study, the geometry optimized lattice constant, Sn-Sn bond length and buckling height of the stanene are 4.687 Å, 2.834 Å and 0.82 Å respectively, which is in good agreement with the reported experimental studies and simulation studies. A 4 × 4 supercell of MoS$_2$ with a 5 × 5 supercell of graphene was considered due to the 23% difference in the lattice constants between graphene (2.42 Å) and MoS$_2$ (3.12 Å) and the graphene layer was further stretched by ~3% to meet the commensurability criterion. Also, Chen et al. investigated the electronic and optical property of graphene/stanene heterobilayers where the lattice constants of graphene and stanene differ by about 46%. Hence, they proposed a supercell composed of 4 × 4 graphene and 2 × 2 stanene and further stretched the stanene layer by 4.7% to form commensurable structures.

Three stacking patterns of stanene-hexagonal boron nitride (Sn/h-BN) have been considered in this study as shown in Fig. 1(a), (b) and (c), respectively. Pattern I exhibits the heterobilayer structure with alternating Sn atoms either right over B atoms or on the top of the centers of BN hexagons. In case of pattern II, alternating Sn atoms are either over the N atoms or on the top of the h-BN centers. In case of pattern III, each of the Sn atoms lies either over the N atom or over the B atom. Similar stacking patterns are reported in the literature for the study of the heterobilayer structures such as graphene/h-BN, graphene on copper substrate, germanene/BeO and graphene/stanene.

Figure 2 represents the binding energies per unit cell with the variation of the interlayer distance for the three considered configurations. Obtained equilibrium distances are 3.75 Å, 3.78 Å and 3.7 Å for structure I, II and III, respectively. For the benchmarking of our calculation, we have computed the optimized interlayer distance of the graphene/h-BN heterobilayer. Our computed equilibrium interlayer distance using DFT for the graphene/h-BN heterobilayer is 2.53 Å, which is in close proximity with the reported value (2.58 Å) by Ukpong et al. for graphene/h-BN heterobilayer. Our obtained equilibrium distances are also comparable to the reported interlayer distances (3.57 Å to 3.75 Å) for bilayer h-BN using GGA in the scheme of PBE. It is also comparable to the experimentally obtained interlayer distance of the Sn bilayers (3.5 Å ± 0.2 Å) during the epitaxial growth of stanene as well as with the calculated interlayer distance of the Sn bilayers (3.6 Å) by Evazzade et al. using GGA and PBE exchange correlation in the Quantum Espresso package where DFT-D modeling has been employed. On the other hand, vdW-DF2 has been reported to yield an equilibrium interlayer distance higher than the experimentally determined interlayer distance for some heterobilayers (3.77 Å for graphene-SiC) in fact, the equilibrium interlayer distance is found to be sensitive with the choice of the exchange-correlation functionals.

Moreover, as suggested by the binding energies of the three configurations shown in Fig. 2, all the considered configurations of the stanene/h-BN heterobilayers are electronically stable while structure I having the lowest binding energy. This can be attributed to the position of the B cations right under the Sn atoms of the stanene.
layer where $\pi$ electron density is high, thereby enhancing the cation-$\pi$ attractive interaction. On the contrary, in structure II, the N anions lie directly under the Sn atoms where the anion-$\pi$ repulsive interaction occurs, thereby leading to a higher binding energy$^{15}$.

Furthermore, the calculated binding energies in our study for the Sn/h-BN heterobilayers per unit cell at equilibrium are more than 250 meV which is higher$^{14,41}$ than the binding energies of the weak vdW interactions$^{42}$. This indicates that the stanene monolayer is bound to the h-BN substrate via interactions somewhat stronger than the weak vdW interactions$^{43}$. The heterobilayers such as graphene/h-BN$^{15,36}$, stanene/MoS$_2$ $^{44}$ and graphene/SiO$_2$ $^{42}$ are reported to have weak vdW interactions between the heterobilayers with a binding energy of less than 100 meV per unit cell. On the other hand, in the graphene/HfO$_2$ heterobilayer structures, the graphene is strongly bound to the HfO$_2$ with a binding energy of 110 meV$^{43}$. The similar phenomenon has been reported in the study of the graphene/stanene heterobilayers$^{14}$ with a binding energy of more than 180 meV per unit cell at optimum spacing. As an aside, the optimized interlayer distances for the three stacking configurations of the Sn/h-BN heterobilayers considered in this study are 3.7 Å to 3.78 Å, which are larger than the typical bond length of the Sn-B bonds (2.24 Å)$^{13}$ and the bond length of the Sn-N bonds (2.14 Å)$^{13}$. This indicates that, the Sn-B and the Sn-N covalent

Figure 1. Atomistic model of Sn/h-BN heterobilayers with different stacking patterns. (a) supercell of Pattern I (b) supercell of Pattern II (c) supercell of Pattern III (d) Front view of the unit cell. It has two Sn atoms, four B atoms and four N atoms. ’h’ denotes the buckling height of the stanene layer at equilibrium, which is 0.82 Å.
bonds are absent in the Sn/h-BN heterostructures and further conforms to the similar phenomena reported regarding the graphene/stanene\textsuperscript{14} and the graphene/HfO\textsubscript{2}\textsuperscript{43} heterobilayers.

For further benchmarking, we have computed the band structure of the 2D monolayer stanene without SOC as well as in the presence of SOC as shown in Fig. 3(a) and (b) respectively. As can be seen from Fig. 3(a), 2D stanene is a zero band gap material in the absence of SOC. When SOC is considered, a direct band gap of 69 meV (Fig. 3(b)) is opened at the K point. This is in excellent agreement with the DFT simulation study of 2D monolayer stanene using GGA in the scheme of PBE by Modarresi \textit{et al}.\textsuperscript{45} (70 meV direct band gap in the presence of SOC) as well as by Xiong \textit{et al}.\textsuperscript{46} (73 meV direct band gap with SOC), thereby confirming the validity of our simulations. Furthermore, in the presence of SOC a Fermi-level band crossing phenomenon of bands is observed at gamma (Γ) point. For the band structure of stanene as well as stanene nanoribbons in the presence of SOC, at gamma point similar phenomenon of either bands touching or crossing the Fermi level has been reported by Broek \textit{et al}.\textsuperscript{5, Modarresi \textit{et al}.\textsuperscript{45}, Lu \textit{et al}.\textsuperscript{47}, as well as by Nagarajan \textit{et al}.\textsuperscript{48}. Despite this phenomenon, in view of the opening of the band gap at K point Broek \textit{et al}.\textsuperscript{5} concluded that, pristine stanene offers perspectives of an all-Sn field effect transistor (FET). However, as discussed by Xiong \textit{et al}.\textsuperscript{46} and Nagarajan \textit{et al}.\textsuperscript{48}, the effect of SOC on the band structure of stanene and the Fermi level touching or crossing phenomenon indicates its possibility of applications in spinelectronics and quantum spin Hall fields. Hence, the overall effect of SOC in the band structure of stanene and stanene based nanostructures requires consideration in terms of their promising application in nanoelectronics, spinelectronics, quantum spin Hall insulators as well as field effect transistor.

Figure 4 shows the band structure of the stanene/h-BN heterobilayer without considering the effect of SOC for the three optimized configurations. The Fermi energy level is set to 0. The band structure patterns are almost similar for all the configurations and an opening of direct band gap of 25 meV for structure I, 33 meV for structure II and 30 meV for structure III can be observed at the K point. The magnified band structures around K point...
near the Fermi levels are also shown at the inset. As shown in the figure, linear Dirac dispersion relation is well preserved in all the three structures. Without SOC, pristine stanene shares the similar Dirac feature and no band gap is observed while the studied stanene/h-BN heterobilayer shows a direct band gap that indicates its possible application in nanoelectronic devices such as FETs.

With the inclusion of SOC, the observed band gap for the structure I, II and III are 74 meV, 109 meV and 90 meV, respectively as shown in Fig. 5. The estimated band gaps including the effect of SOC are higher in magnitude with no significant change in the band structures near the K point as can be observed from the magnified plots in Fig. 5. This can be attributed to the effect of SOC on the heavy Sn atoms. In fact, group IV materials such as silicon (Si), tin (Sn) and lead (Pb) with single layer hexagonal configurations show SOC-induced band gaps and this effect gets stronger with the increasing atomic number of heavier atoms49. However, at gamma point (Γ) a Fermi-level band crossing phenomenon of bands can be observed which is similar to pristine stanene with the effect of SOC indicating the possibility of applying Sn/h-BN heterobilayers in the application of spinelectronics and quantum spin Hall insulators46,48.

The linear Dirac dispersion near K point suggests a high charge carrier mobility. To further analyze this fact, we have calculated the effective mass of electrons \(m^*_{e}\) and holes \(m^*_{h}\) at the Dirac point for the three (3) configurations of stanene/h-BN heterobilayer. For structure III, the calculated effective mass for the electron \(m^*_{e}\) and the hole \(m^*_{h}\) are 0.0507 \(m_0\) and 0.0543 \(m_0\), respectively, which are small enough to provide high carrier mobility. The computed electron effective masses for the other two configurations are 0.054 \(m_0\) (structure I) and 0.0513 \(m_0\) (structure II). On the other hand, the calculated Fermi velocities are 0.538 \(\times 10^6\) ms\(^{-1}\), 0.526 \(\times 10^6\) ms\(^{-1}\) and 0.538 \(\times 10^6\) ms\(^{-1}\) for structure I, II and III, respectively which are in the similar order of magnitude to that of stanene5 (0.97 \(\times 10^6\) ms\(^{-1}\)) and graphene50 (106 ms\(^{-1}\)).

Due to the interaction between the stanene and the h-BN layer, the sublattice symmetry of the zero band gap hexagonal stanene structure is broken, therefore opening a direct band gap. Similar phenomenon has been reported by Xiong et al.34 for the stanene/MoS\(_2\) heterostructure where the strong interaction breaks the sublattice symmetry of stanene and opens a band gap. Similarly, the strong interaction with the BeO monolayer substrate introduces a finite band gap in the germanene/BeO heterostructure by breaking the symmetry of the germanene37. Also, due to the symmetry breaking of the two carbon atoms in the hexagonal graphene induced by the interaction with the h-BN monolayer, a finite band gap of ~50 meV opens as reported in the literature15,36.

Figure 4. Band structures and the magnified band structures around K point of stanene/h-BN heterostructure without SOC (a) structure I (b) structure II (c) structure III.
Next, to analyze the electronic properties and gain deeper insight on the interlayer interactions, we have plotted the total as well as the projected density of states (PDOS) for structure III of the stanene/h-BN heterobilayer as shown in Fig. 6. As all the considered configurations of the Sn/h-BN heterobilayer are found to show similar band structure along with nearly same energy band gap, effective mass as well as Fermi velocity, hence we show the results for structure III only as a representative of Sn/h-BN heterobilayer. As depicted in Fig. 6(a), the peaks...
of the PDOS in the conduction band (0 to 2 eV) as well as in the valence band (−2 to 0 eV) are dominantly contributed by stanene. Again, molecular orbital resolved density of states presented in Fig. 6(b) reveals the dominant role of the π orbital of stanene in the conduction and valence bands, which is similar to the characteristics of the isolated monolayer stanene. Furthermore, as shown in Fig. 6, unlike hybrid systems with high chemical interactions, h-BN orbitals do not hybridize with stanene orbitals near the Fermi level ensuring non-intensive interactions of the two layers. This is further supported by the real space charge density distribution of the conduction and valence bands for structure III as shown in Fig. 7. The localization of stanene in the conduction band as well as in the valence band of the heterobilayer structure further confirms the dominant role of stanene in shaping the electronic properties of the stanene/h-BN heterostructure. Therefore, electronic carriers are expected to transport only through the stanene layer, thereby leaving the h-BN layer to be a good choice as a substrate for the heterostructure. The localization of stanene in the conduction band and the valence band of the Sn/h-BN heterobilayer structure in this study can be compared to the heterostructures formed by other group-IV mono atomic 2D compounds such as graphene and silicene with h-BN working as a substrate. As reported by Balu et al., the band structure for the graphene/BN bilayer is dominated by the bands associated with the carbon atoms near the Fermi level, with a band gap of ~100 meV at the Dirac point. Similarly, silicene is reported to dominate the electronic transport in the silicene/h-BN heterobilayers and the Dirac cone of the silicene layer is preserved after contacting the BN layer, which is in accordance with our study for the stanene/h-BN heterobilayers. In fact, the heterostructures consisting of single layer silicene and graphene sandwiched between h-BN bilayers also show a band gap opening and high carrier mobility while the silicene and graphene layer remain nearly unaffected by h-BN. In addition, the periodic heterostructures with a graphene sheet sandwiched between four h-BN layers also show similar phenomenon.

In this section, we focus our study to tune up the band gap of the Sn/h-BN heterostructure for its possible use in the high performance nano electronic and spintronic devices.

Firstly, we have calculated the energy band gaps with the variation of the interlayer spacing of the stanene and h-BN layers for all three considered configurations as presented in Fig. 8. With the increasing interlayer distance, energy band gap decreases. As the interlayer distance increases, the interaction between the h-BN and stanene layer decreases. As a result, the stanene layer tends to get back to its original symmetry therefore reducing the band gap. This is in line with the study of graphene/h-BN heterobilayers of various stacking patterns where the band gaps increase with the decrease in interlayer spacing.

Figure 9 shows the variation in the band gap for structure III under external strain of varying percentage. The strain ε is defined as the following:

$$\varepsilon = \frac{a_{\text{strained}} - a_{\text{relaxed}}}{a_{\text{relaxed}}} \times 100$$

where, a is the unit cell parameter. For the applied biaxial strain, the structural symmetry remains almost same as the unstrained case thereby causing a little increase in the band gap as shown in Fig. 9(a). The small changes in the effective mass and the Fermi velocities are also presented in Fig. 9(a). With the increasing percentage of strain, the Fermi level shifts downward and a self hole doping characteristics with hole carriers appear, which is evident in Fig. 9(b). In fact, at a strain of 4%, the Fermi level touches the valence band and further shifts downward at a maximum strain of 7%. This is also in line with the study for the stanene monolayer. On the other hand, the reverse phenomenon i.e. the upward shift of Fermi level is expected for the compressive strain.

Finally, we have investigated one non-high symmetry configuration for the Sn/h-BN heterostructure as shown in Fig. 10(a). For the considered non-high symmetry supercell structure, the supercell is made up of $\sqrt{7} \times \sqrt{7}$ stanene and $5 \times 5$ h-BN and the stanene layer is rotated by 21.5° with respect to the h-BN layer which ensures the commensurability condition in the supercell.
The electronic band structure for the non-high symmetry configuration is shown in Fig. 10 (b). A direct band gap of ~20 meV can be observed at M point which is comparable to the obtained band gap of ~30 meV for the high symmetry configurations of the Sn/h-BN heterobilayer in this study. Hence, it is reasonable to conclude that, non-high symmetry configurations will not substantially reduce the band gap of the Sn/h-BN heterobilayers. This is in accordance with the findings for graphene/h-BN heterobilayers as reported by Giovannetti et al.36.

Conclusion
In summary, we have investigated the structural and electronic properties of the Sn/h-BN heterobilayers from DFT studies considering van der Waals interaction between two layers. We have considered three different stacking patterns and all of these are found to be electrically stable in terms of the high binding energy. The band structures of the Sn/h-BN heterobilayer shows a direct band gap of about 30 meV at the Fermi energy level while linear Dirac dispersion relation is closely maintained. The real space charge distribution and density of states of the heterostructure suggest the localization of stanene $\pi$ orbital in the conduction as well as in the valence bands, further confirming the superior role of stanene in shaping the electronic properties of the stanene/h-BN heterostructure. Moreover, our calculated small
8. Zhu, F.-F. 
9. Xu, Y. 
11. Liu, C. C., Jiang, H. & Yao, Y. Low-energy effective Hamiltonian involving spin-orbit coupling in silicene and two-dimensional 
13. Garg, P., Choudhuri, I., Mahata, A. & Pathak, B. Band gap opening in stanene induced by patterned B–N doping. 
14. Chen, X. 
10. Wang, D., Chen, L., Wang, X., Cui, G. & Zhang, P. The effect of substrate and external strain on electronic structures of stanene film. 
12. Wang, J., Xu, Y. & Zhang, S. C. Two-dimensional time-reversal-invariant topological superconductivity in a doped quantum spin-
6. Manjanath, A., Kumar, V. & Singh, A. K. Mechanical and Electronic Properties of pristine and Ni-doped Si, Ge, and Sn sheets. 
7. Xiong, W. 
16. Slawinska, J., Zasada, I. & Klusek, Z. Energy gap tuning in graphene on hexagonal boron nitride bilayer system. 
17. Lu, Y. H., He, P. M. & Feng, Y. P. Asymmetric Spin Gap Opening of Graphene on Cubic Boron Nitride (111) Substrate. J. Phys. Chem. C 112, 12683–12686 (2008). 
18. Balu, R., Zhong, X., Pandey, R. & Karns, S. P. Effect of electric field on the band structure of graphene/boron nitride and boron nitride/boron nitride bilayers. Appl. Phys. Lett. 100, 21–23 (2012). 
19. Giannozzi, P. et al. Quantum ESPRESSO: a modular and open-source software project for quantum simulations of materials. J. Phys. Condens. Matter 21, 395502 (2009). 
20. Troullier, N. & Martins, J. L. Efficient pseudopotentials for plane-wave calculations. Phys. Rev. B 43, 8861–8869 (1991). 
21. Perdew, J. P., Burke, K. & Ernzerhof, M. Generalized Gradient Approximation Made Simple. Phys. Rev. Lett. 77, 3865–3868 (1996). 
22. Lee, K., Murray, É. D., Kong, L., Lundqvist, B. I. & Langreth, D. C. Higher-accuracy van der Waals density functional. Phys. Rev. B 82, 3–6 (2010). 
23. Grimme, S. Valence Bond Theory for Chemical Dynamics. J. Comput. Chem. 28, 73–86 (2009). 
24. Saxena, S., Choudhary, R. P. & Shukla, S. Stanene: Atomically Thick Free-standing Layer of 2D Hexagonal Tin. Sci. Rep. 6, 1–4 (2015). 
25. García, J. C., Lima, D. B., De, Assali, L. V. C. & Justo, F. Group IV Graphene- and Graphene-Like Nanosheets. J. Phys. Chem. C 115, 13242–13246 (2011).

effective mass and the emergence of Dirac cone suggest high charge carrier mobility for the Sn/h-BN heterostructure. Furthermore, our analysis concludes that, the band gap can be effectively tuned by varying the interlayer spacing between the Sn and h-BN monolayer while preserving the stability. A small increase in the band gap is observed with the increasing percentage of tensile biaxial strain. At a higher percentage of strain, the Fermi level shifts downward and self hole doping characteristics with hole carriers appear. Such unique and tunable electronic properties of the Sn/h-BN heterobilayer would further encourage the Sn-based nanoelectronic and spintronic device applications.

**References**

1. Ferrari, A. C. et al. Science and technology roadmap for graphene, related two-dimensional crystals, and hybrid systems. Nanoscale 7, 4598–4810 (2014). 
2. Ezawa, M. Photo-Induced Topological Superconductor in Silicene, Germanene, and Stanene. J. Supercond. Nov. Magn. 28, 1249–1253 (2015). 
3. Rachel, S. & Ezawa, M. Giant magnetoresistance and perfect spin filter in silicene, germanene, and stanene. Phys. Rev. B 89, 1–6 (2014). 
4. Li, S. et al. First-order magnetic and structural phase transitions in Fe1+ x Se1–x. Phys. Rev. B 79, 1–7 (2009). 
5. Broek, B. van den et al. Two-dimensional hexagonal tin: ab initio geometry, stability, electronic structure and functionalization. 2D Mater. 1, 21004 (2014). 
6. Manjanath, A., Kumar, V. & Singh, A. K. Mechanical and Electronic Properties of pristine and Ni-doped Si, Ge, and Sn sheets. Phys. Chem. Chem. Phys. 16, 1667–1671 (2014). 
7. Xiong, W. et al. Tuning electronic structures of the stanene monolayer via defects and transition-metal-embedding: spin–orbit coupling. Phys. Chem. Chem. Phys. 18, 28759–28766 (2016). 
8. Zhu, F. et al. Epitaxial growth of two-dimensional stanene. Nat. Mater. 14, 1020–1025 (2015). 
9. Xu, Y. et al. Large-gap quantum spin hall insulators in tin films. Phys. Rev. Lett. 111, 1–5 (2013). 
10. Wang, D., Chen, L., Wang, X., Cui, G. & Zhang, P. The effect of substrate and external strain on electronic structures of stanene film. Phys. Chem. Chem. Phys. 17, 26979–26987 (2015). 
11. Liu, C. C., Jiang, H. & Yao, Y. Low-energy effective Hamiltonian involving spin-orbit coupling in silicene and two-dimensional germanium and tin. Phys. Rev. B 84, 1–11 (2011). 
12. Wang, J., Xu, Y. & Zhang, S. C. Two-dimensional time-reversal-invariant topological superconductivity in a doped quantum spin-Hall insulator. Phys. Rev. B 90, 1–5 (2014). 
13. Garg, P., Choudhuri, I., Mahata, A. & Pathak, B. Band gap opening in stanene induced by patterned B–N doping. Phys. Chem. Chem. Phys. 19, 3660–3669 (2017). 
14. Chen, X. et al. Electronic structure and optical properties of graphene/stanene heterolayer. Phys. Chem. Chem. Phys. 18, 16302–16309 (2016). 
15. Fan, Y., Zhao, M., Wang, Z., Zhang, X. & Zhang, H. Tunable electronic structures of graphene/boron nitride heterobilayers. Appl. Phys. Lett. 98, 5–8 (2011). 
16. Slawinska, J., Zasada, I. & Klusek, Z. Energy gap tuning in graphene on hexagonal boron nitride bilayer system. Phys. Rev. B 81, 1–9 (2010). 
17. Lu, Y. H., He, P. M. & Feng, Y. P. Asymmetric Spin Gap Opening of Graphene on Cubic Boron Nitride (111) Substrate. J. Phys. Chem. C 112, 12683–12686 (2008).
26. Wang, J. Large-Gap Quantum Spin Hall Insulators in Tin Films. *Phys. Rev. Lett.* **111**(136804), 1–6 (2013).
27. Khan, A. I., Paul, R. & Subrina, S. Thermal transport in graphene/stanene hetero-bilayer nanostructures with vacancies: an equilibrium molecular dynamics study. *RSC Adv.* **7**, 44780–44787 (2017).
28. Nissimagoudar, A. S., Manj Nathan, A. & Singh, A. K. Diffusive nature of thermal transport in stanene. *Phys. Chem. Chem. Phys.* **18**, 14257–14263 (2016).
29. Peng, B. et al. Low lattice thermal conductivity of stanene. *Sci. Rep.* **6**, 2–11 (2016).
30. Wang, J., Ma, F. & Sun, M. Graphene, hexagonal boron nitride, and their heterostructures: properties and applications. *RSC Adv.* **7**, 16801–16822 (2017).
31. Catelani, A., Posternak, M., Balderschi, A., Jansen, H. J. F. & Freeman, A. J. Electronic interlayer states in hexagonal boron nitride. *Phys. Rev. B* **32**, 6997–6999 (1985).
32. Ukppong, A. M. First principles study of van der Waals heterobilayers. *Comput. Condens. Matter* **2**, 1–10 (2015).
33. Khan, A. I., Navid, I. A., Noshin, M. & Subrina, S. Thermal transport characterization of hexagonal boron nitride nanoribbons using molecular dynamics simulation. *AIP Adv.* **7**, 105110 (2017).
34. Liu, B. et al. Thermal transport in a graphene–MoS2 bilayer heterostructure: a molecular dynamics study. *RSC Adv.* **5**, 29193–29200 (2015).
35. Liu, X. & Li, Z. Electric Field and Strain Effect on Graphene-MoS2 Hybrid Structure: Ab Initio Calculations. *J. Phys. Chem. Lett.* **6**, 3269–3275 (2015).
36. Giovannetti, G., Khomyakov, P. A., Brockgs, G., Kelly, P. J. & Brink, J. Van Den. Substrate-induced band gap in graphene on hexagonal boron nitride: Ab initio density functional calculations nitrogen boron carbon. *Phys. Rev. B* **76**, 1–4 (2007).
37. Sun, X., Jiang, J., Liang, Q., Yang, Q. & Meng, R. The Electrical and Optical Properties of Germanene on Single-Layer BeO Substrate. The electrical and optical properties of germanene on single-layer BeO substrate. *J. Phys. Chem. C* **120**(36), 20350–20356 (2016).
38. Ribeiro, R. M. & Peres, N. M. R. Stability of boron nitride bilayers: Ground-state energies, interlayer distances, and tight-binding description. *Phys. Rev. B* **83** (2011).
39. Evzazade, I. et al. Semimetal behavior of bilayer stanene. *Phys. E Low-Dimensional Syst. Nanostructures* **89**, 155–159 (2017).
40. Wei, C.-R. H., C.-P., J.-P., C.-M. C. & C.-M. Van der Waals interaction in a boron nitride nanoribbon using molecular dynamics. *AIP Adv.* **7**, 105110 (2017).
41. Liu, Z. et al. Impurity Resonant States p-type Doping in Wide-Band-Gap Nitrides. *Sci. Rep.* (613957), 1–8 (2016).
42. Nguyen, T. C., Otani, M. & Okada, S. Semiconductor Electronic Property of Graphene Adsorbed on (0001) Surfaces of SiO2. *Phys. Rev. Lett.* **106**, 106801 (2011).
43. Kamiya, K., Umezawa, N. & Okada, S. Energetics and electronic structure of graphene adsorbed on H2O (111): Density functional theory calculations. *Phys. Rev. B* **83**(154313), 1–4 (2011).
44. Ren, C.-C., Feng, Y., Zhang, S.-F., Zhang, C.-W. & Wang, P.-J. The electronic properties of the stanene/MoS2 heterostructure under strain. *RSC Adv.* **7**, 9176–9181 (2017).
45. Modarresi, M., Kakoee, A., Mogulkoc, Y. & Roknabadi, M. R. Effect of external strain on electronic structure of stanene. *Comput. Mater. Sci.* **101**, 164–167 (2015).
46. Xiong, W. et al. Spin-orbit coupling effects on electronic structures in stanene nanoribbons. *Phys. Chem. Chem. Phys.* **18**, 6534–6540 (2016).
47. Lu, F. et al. Quasiparticle and optical properties of strained stanene and stanane Results Geometric structure. *Sci. Rep.* **7**(3912), 1–8 (2017).
48. Nagarajan, V. & Chandiramouli, R. Investigation of electronic properties and spin-orbit coupling effects on passivated stanene nanosheet: A first-principles study. *Superlattices Microstruct.* **107**, 118–126 (2017).
49. Zhang, S., Ji, W., Zhang, C., Li, P. & Wang, P. Two-Dimensional Large Gap Topological Insulators with Tunable Rashba Spin-Orbit Coupling in Group-IV films. *Sci. Rep.* **7**, 45923 (2017).
50. Novoselov, K. S. et al. Two-dimensional gas of massless Dirac fermions in graphene. *Nature* **438**, 197–200 (2005).
51. Xiong, W. et al. Band engineering of the MoS2/stanene heterostructure: strain and electrostatic gating. *Nanotechnology* **28**, 195702 (2017).
52. Hu, W., Li, Z. & Yang, J. Electronic and optical properties of graphene and graphitic ZnO nanocomposite structures. *J. Chem. Phys.* **138** (2013).
53. Cai, Y., Pei, Q., Zhang, G. & Zhang, Y. Decoupled electron and phonon transports in hexagonal boron nitride-silicene bilayer heterostructure. *J. Appl. Phys.* **119** (2016).
54. Ni, Z. et al. Tunable Bandgap in Silicene and Germanene. *Nano Lett.* **12**, 113–118 (2012).
55. Quhe, R. et al. Tunable and sizable band gap of single-layer graphene sandwiched between hexagonal boron nitride. *NPG Asia Mater.* **4**, 1–11 (2012).
56. Aggoun, W. et al. Enhanced Light–Matter Interaction in Graphene/h-BN van der Waals Heterostructures. *J. Phys. Chem. Lett.* **8**, 1464–1471 (2017).
57. Li, L. & Zhao, M. Structures, energetics, and electronic properties of multifarious stacking patterns for high-buckled and low-buckled silicene on the MoS2 substrate. *J. Phys. Chem. C* **118**, 19129–19138 (2014).
58. Li, L., Wang, X., Zhao, X. & Zhao, M. More superstructures of silicene on hexagonal boron nitride: A first-principles study. *Phys. Lett. Sect. A* *Gen. At. Solid State Phys.* **377**, 2626–2632 (2013).

**Author Contributions**
A.I.K. conceived the work; A.I.K., T.C. and N.A. performed the simulations under the supervision of S.S. All authors discussed and analyzed the data and interpretation and contributed during the writing of the manuscript.

**Additional Information**

**Competing Interests:** The authors declare that they have no competing interests.

**Publisher’s note:** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

© The Author(s) 2017