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Low transverse emittance electron bunches from two-color laser-ionization injection

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ABSTRACT

A method is proposed to generate low emittance electron bunches from two color laser pulses in a laser-plasma accelerator. A two-region gas structure is used, containing a short region of a high-Z gas (e.g., krypton) for ionization injection, followed by a longer region of a low-Z gas for post-acceleration. A long-laser-wavelength (e.g., 5 \( \mu \)m) pump pulse excites plasma wake without triggering the inner-shell electron ionization of the high-Z gas due to low electric fields. A short-laser-wavelength (e.g., 0.4 \( \mu \)m) injection pulse, located at a trapping phase of the wake, ionizes the inner-shell electrons of the high-Z gas, resulting in ionization-induced trapping. Compared with a single-pulse ionization injection, this scheme offers an order of magnitude smaller residual transverse momentum of the electron bunch, which is a result of the smaller vector potential amplitude of the injection pulse.

Keywords: two color lasers, ionization injection, laser wakefield, transverse momentum, transverse emittance

1. INTRODUCTION

In laser-driven plasma-based accelerators (LPAs)\textsuperscript{[2]} the accelerating and focusing fields (wakefields) are driven by the ponderomotive force of the laser pulse \( F \sim \nabla a^2 \), where \( a^2 = 7.3 \times 10^{-19}[\lambda(\mu \text{m})]^2 I/(\text{Wcm}^{-2}) \) (linear polarization) is the normalized laser intensity, \( a = eA/m_c c^2 \) is the normalized amplitude of the laser vector potential, and \( \lambda \) is the laser wavelength in vacuum. The accelerating field is on the order of \( E(\text{V/m}) \approx 96 \sqrt{n_0}(\text{cm}^{-3}) \) with \( n_0 \) the plasma electron density, which can be several orders of magnitude greater than those in conventional accelerators. In addition, LPAs have the potential to produce extremely short electron bunches with durations \( \tau_b < \lambda_p/c \), where \( \lambda_p(\mu \text{m}) \approx 3.3 \times 10^{10}/\sqrt{n_0}(\text{cm}^{-3}) \) is the plasma wavelength. In 2004, high-quality electron bunches with energy \( \sim 100 \text{ MeV} \) were produced\textsuperscript{[11]} with significant charge (\( > 100 \text{ pC} \)), small energy spread (<10%), and low divergence (few mrad). In 2006, high-quality GeV-class electron beams were first demonstrated by using a capillary plasma-channel guided laser in cm-scale plasma\textsuperscript{[25]} Controlled injection methods, such as colliding pulses injection\textsuperscript{[26]} density transitions\textsuperscript{[18,27]} and ionization injection\textsuperscript{[26,28]} are actively being pursued to improve the quality and stability of the electron beams. Experiments have so far successfully demonstrated production of electron bunches with energy spread at \( \sim 1\% \)\textsuperscript{[11,22]} and estimated transverse emittance at \( \sim 0.1 \text{ mm mrad} \)\textsuperscript{[23]} Such high-quality electron beams could be good candidates to drive free-electron lasers (FELs)\textsuperscript{[23]} which provide a new generation of low-cost, compact light sources\textsuperscript{[23,24]}. Further decreasing the transverse emittance is critical to many applications of the high-energy electron beams, such as drivers future x-ray FELs.

The normalized transverse emittance can be estimated as \( \epsilon_x \sim \sigma_x \sigma_{p_x}/(m_c c) \), where \( \sigma_x \) is the root-mean-square (rms) bunch radius and \( \sigma_{p_x}/(m_c c) \) is the normalized rms transverse momentum. In the self-trapping bubble regime, simulations show \( \sigma_x \sim 0.1 \mu \text{m} \) and \( \sigma_{p_x}/(m_c c) \sim 1 \), resulting in \( \epsilon_x \sim 0.1 \text{ mm mrad} \)\textsuperscript{23} Recently, simulations show that an electron bunch with excellent normalized emittance (0.04 mm mrad) can be produced via laser ionization in a beam-driven plasma bubble regime\textsuperscript{[24]}. In this scheme, a mixture of Li and He gas is used.

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Figure 1. (Color online) Concept of two-color laser-ionization injection. The high-Z gas is krypton. (a) The vector potentials of the pump pulse $a_0$ (with $\lambda_0 = 5 \mu m$) and injection pulse $a_1$ (with $\lambda_1 = 0.4 \mu m$) (black curves) and the normalized excited wakefield $eE_0/mc\omega pc$ (red curve). (b) The electric fields of the pump pulse $E_0$ and injection pulse $E_1$ (black curves) and the ionization degree of $K_{8+}^r \rightarrow K_{9+}^r$ (green curve). (c) Schematic profile of the longitudinal density. Electron density $n_0(x) = n_e(x) + 8n_{Kr}(x)=$constant.

An electron beam is propagating in the gas mixture with fully-ionized Li, generating an intense Li plasma bubble. The electric field of the electron beam driver is chosen not high enough to ionize the He gas. A tightly-focused (laser spot size $w_0 = 4 \mu m$) nonrelativistic-intensity ($a_0=0.018$) laser pulse is used to ionize He component and release electrons directly into the accelerating and focusing phase of the Li plasma bubble. Assuming the produced electron rms bunch radius is $\sim w_0/\sqrt{2}$ and the normalized rms transverse momentum is $\sim a_0/2$, the expected minimal emittance is $\sim w_0 a_0/2^{3/2}$. In contrast, conventional methods for ionization injection in LPAs, where $a_0 \sim 2$ and $w_0 \sim 10 \mu m$ are needed to drive the wake, typically produce emittances of a few mm mrad.

Here we propose a method to generate low-emittance high-quality electron bunches in a laser-plasma accelerator. As shown in Fig. (a) and (b), a long-wavelength (e.g., 5 $\mu m$) pump pulse with an amplitude $a_0 \simeq 1$ propagates in a high-Z gas (e.g., krypton) and ionizes the gas to a mid-charge state, exciting an intense wakefield. The electric field of the pump pulse $E_0$ is relatively low due to the long laser wavelength $a = eE\lambda/(2\pi m_e c^2)$, so that it cannot ionize the high-ionization-threshold electrons. A short-wavelength (e.g., 0.4 $\mu m$) injection pulse with an amplitude $a_1 \sim 0.15$ is used to ionize the high-ionization-threshold electron (e.g., $K_{8+}^r \rightarrow K_{9+}^r$) because of the higher electric field $E_1 > E_0$. The electrons ionized by the injection pulse at proper wake phases can be trapped and be accelerated to high energy. The gas structure used in the Particle-In-Cell (PIC) simulations in this paper is shown in Fig. (c). A high-Z gas (krypton) is used for the ionization injection and a low-Z gas is used for the post-acceleration without additional trapping. This two-region gas structure allows us to control the injection number and beam quality of the electron bunch by changing the gas composition, concentration, and length of the high Z gas region. The total ionized electron number (until the 8th electron of krypton) is fixed and the electron density is set to be $n_0(x) = n_e(x) + 8n_{Kr}(x)=$constant, so that the density ramp effects are negligible. The normalized rms transverse momentum of the injected electrons in this scheme is $\sim 0.03$, which is an order of magnitude smaller than that in a single pulse ionization injection.

This paper is organized as follows. Section 2 presents the high-Z gas selection and the trapping condition for the ionized electron by using a Hamiltonian approach. Section 3 presents one-dimensional (1D) PIC simulations of the ionization injection. Section 4 gives the conclusions and a discussion of multi-dimensional effects.
2. HIGH-Z GAS SELECTION AND ELECTRON TRAPPING CONDITION

In a single laser pulse ionization injection, typically the peak of the laser pulse is at \( a_0 \sim 2 \) for a resonant Gaussian laser pulse and uses an appropriate high-Z gas (e.g., nitrogen), with a laser wavelength of 0.8 µm\(^2\)\(^3\). In this case, ionization injection requires two conditions: (1) the laser intensity needs to be intense enough to excite a sufficiently large wakefield so that an electron ionized at rest near the peak intensity of the laser pulse will be on a trapped orbit; and (2) the ionization threshold of the inner shell electron of the high-Z gas needs to be close to the laser pulse intensity peak.

In the two-color laser-ionization injection scheme, \( a_1 \) can be delayed to a position in the wake with a lower trapping threshold. Once the electron is born at rest in the wake phase where the separatrix is negative, it can be trapped. In order to achieve a small transverse emittance of the electron bunch, the amplitude \( a_1 \) needs to be as small as possible. Thus, an appropriate gas needs to be chosen so that the pump pulse will not trigger the electron to be close to the laser pulse intensity peak.

2.1 Electron Dynamics and Trapping Condition

The nonlinear plasma wave generated by the intense circularly-polarized pump pulse in cold underdense plasma in 1D limit can be written as\(^4\)

\[
k_p^2 \frac{\partial^2 \phi}{\partial \xi^2} = \gamma_p^2 \left\{ \beta_p \left[ 1 - \frac{1 + a_0^2}{\gamma_p^2(1 + \phi)} \right]^{1/2} - 1 \right\},
\]

(1)

Here \( \xi = z - v_p t \) is forward co-moving coordinate, \( \phi(\xi) = e\Phi/mc^2 \), \( k_p = 2\pi/\lambda_p \) and \( \beta_p = v_p/c \) are the normalized potential, the wave number and the normalized phase velocity of the plasma wave, respectively. In underdense plasma \( \beta_p \approx \beta_g \approx 1 \) with \( \beta_g \) the group velocity of the laser pulse. \( \gamma_p = (1 - \beta_p^2)^{-1/2} \), and \( a_0(\xi) \) is the pump pulse profile. The normalized wakefield is \( E_z e/(m_e \omega_p c) = -k_p^2 \partial \phi / \partial \xi \). In the absence of the pump pulse, the electron motion in the plasma wake can be described using a Hamiltonian approach\(^2\)

\[
H(u_z, \psi) = (1 + u_z^2)^{1/2} - \beta_p u_z - \phi(\psi),
\]

(2)

where \( \psi = k_p \xi \) is the wake phase and \( u_z = p_z/m_e c \) is the normalized longitudinal momentum of the electron. The separatrix orbit between trapped and untrapped orbits is given by \( u_z = u_z(H_s(\gamma_p, \psi_{\text{min}})) \), where \( \phi(\psi_{\text{min}}) = \phi_{\text{min}} \) and \( H_s = 1/\gamma_p - \phi_{\text{min}} \). For the electron ionized inside the injection pulse, the Hamiltonian can be written as\(^2\)

\[
H_i = 1 - \phi(\psi_i),
\]

(3)

assuming that the electron is born at rest and \( a_1^2 \ll 1 \). Here \( \psi_i \) is the wake phase. The wake induced by the injection pulse is neglected since it is typically much smaller than \( \phi \). Once the ionized electron lies above the wake separatrix, it can be trapped. Thus, the trapping condition for the ionized electron is

\[
H_i \leq H_s.
\]

(4)

By numerically solving Eq. (1)-(4), we obtain the Hamiltonian of the wake separatrix and the ionized electron, as shown in Fig. 2. Here the initial uniform electron density is \( n_0 = 2 \times 10^{17} \text{ cm}^{-3} \), and the pump laser pulse is circularly polarized with a Gaussian profile \( a_0(\xi) = a_0 \exp[-(\xi - \xi_0)^2/\xi_0^2] \) with \( a_0 = 1 \). The laser wavelength of the pump pulse is \( \lambda_0 = 5 \mu\text{m} \). The length of the pump pulse is matched with the plasma density to maximize the amplitude of the wakefield by setting \( k_p \xi_0 = 2 \) and the FWHM duration of the pump pulse is \( \tau_0 = 92 \text{ fs} \). As shown in Fig. 2, the initial ionization phase for trapping is where \( H_s - H_i > 0 \), and the optimal ionization phase is where \( H_s - H_i \) is maximum. The intensity threshold of the pump pulse for trapping at this phase is \( a_{0,\text{th}} = 0.88 \). The green curve shows the ionization degree of \( K^+ \rightarrow K^+ \) for the injection pulse. Here the injection pulse is linearly polarized and has the same profile as the pump pulse. The amplitude, wavelength and duration (FWHM) of the injection pulse are \( a_1 = 0.15 \), \( \lambda_1 = 0.4 \mu\text{m} \) and \( \tau_1 = 16 \text{ fs} \), respectively. It is found that the ionization phase of the injection pulse meets the trapping condition and all the ionized electrons will be
trapped in the wake. However, the ionization phase of the pump pulse is where $H_s - H_i < 0$ (blue curve), which does not satisfy the trapping condition. Thus, there is no ionization injection from the pump pulse.

The normalized transverse momentum of the ionized electron is $u_\perp(\psi) = p_\perp/m_e c = a_{1,\perp}(\psi) - a_{1,\perp}(\psi_i)$. Most of the electrons are born at the peak electric field of the laser pulse where $a_{1,\perp}(\psi_i) \equiv 0$, while some of the electrons are born off-peak with a finite $a_{1,\perp}(\psi_i)$. Assuming the electron is trapped behind the injection laser pulse, i.e., $a_{1,\perp}(\psi) = 0$, then the transverse momentum is $u_\perp(\psi) = a_{1,\perp}(\psi_i)$. This is the residual transverse momentum that results from the electron being born off-peak of the laser pulse, which contributes the initial transverse emittance of the electron bunch.

### 2.2 High-Z Gas Selection

By using direct current (DC) tunneling ionization model we found that krypton gas may be used for the two- color laser-ionization injection scheme with the pump laser wavelength $\lambda_0 = 5 \mu m$ and the injection laser wavelength $\lambda_1 = 0.4 \mu m$. The laser parameters are the same as presented in Fig. 2. The ionization potential (IP) of the 8th (IP 126 eV) electron of krypton that produces $K^{9+}$ is quite low, so that both the pump pulse and injection pulse can fully ionize the gas up to this shell. However, for the 9th (IP 230 eV) electron of Krypton that produces $K^{9+}$, the ionization degree is strongly dependent on the laser vector potential and laser wavelength (i.e., the laser electric field) for the parameters under consideration. As shown in Fig. 3(a), the ionization degrees of $K^{8+} \rightarrow K^{9+}$ for a circularly-polarized pump pulse is $\geq 3$ orders of magnitude smaller than those for a linearly-polarized pump pulse, while keeping the same wake generation in both cases. This is because in order to generate a same wake, the amplitude of a linearly-polarized pulse $a_0$ needs to be $\sqrt{2}$ larger compared to a circularly-polarized pulse, resulting in a much higher ionization degree. Also, the electron motion in a linearly-polarized intense laser pulse with $a_0 > 1$ is more nonlinear than the one in a circularly-polarized laser pulse with $a_0 \leq 1$. Thus, a circularly-polarized pump pulse is chosen in order to avoid the ionization injection in the first bucket of the wakefield. Figure 3(b) shows the ionization degrees of $K^{8+} \rightarrow K^{9+}$ for a linearly-polarized injection pulse. It is found that high ionization degree can be achieved with a small $a_1$ due to the short laser wavelength. For example, the ionization degree is 96% for $a_1 = 0.15$. With the decrease of $a_1$, the ionization degree decreases and the ionized electron number decreases, resulting in a smaller injection number.

![Figure 2](image-url) (Color online) Trapping condition for an ionized electron is $H_s - H_i > 0$. $H_s$ and $H_i$ are the Hamiltonian values of the wake separatrix and the ionized electron, and $H_s - H_i$ is shown as a function of wake phase $\psi$ (red curve). Ionization degree of $K^{8+} \rightarrow K^{9+}$ for the pump pulse with a circular polarization (blue curve) and for the injection pulse with a linear polarization (green curve). The laser pulses have Gaussian profiles $a(x) = a_{0,1} \exp[-(\xi - 3L_{0,1})^2/L_{0,1}]$, with $a_0 = 1$ and $a_1 = 0.15$. The laser wavelengths are $\lambda_0 = 5 \mu m$ and $\lambda_1 = 0.4 \mu m$, and the pulse durations (FWHM) are $\tau_0 = 1.1774L_0/c = 92$ fs and $\tau_1 = 1.1774L_1/c = 16$ fs. The electron density is $n_0 = 2 \times 10^{17} \text{ cm}^{-3}$.

![Figure 3](image-url)
3. PARTICLE-IN-CELL SIMULATIONS

The two-color laser-ionization injection was examined via 1D PIC simulations using the WARP code. In order to save computational time, a mix of pre-ionized electrons and neutral krypton gas is used, as presented in Fig. 1(c). The initial electron density \( n_0 \) is fixed to \( n_0 = n_e + 8n_{Kr} = 2 \times 10^{17} \text{ cm}^{-3} \) (a plasma wavelength of 75 \( \mu \text{m} \)). The concentration of the krypton in the simulations is set to \( n_{Kr}/n_0 = 1\% \). The length of the trapezoid-shaped krypton gas is 100 \( \mu \text{m} \) with a plateau of 50 \( \mu \text{m} \). The profiles and durations of the two lasers are the same as described in Fig. 2. As discussed above, since the ionization degree of \( K_{r}^{8+} \rightarrow K_{r}^{9+} \) is much smaller for the circularly-polarized pump pulse, we use a circularly-polarized pump pulse with \( a_0 = 1 \) in the simulations. The peak of the pump pulse is located at \( z = 0 \). Figures 4(a)-(c) shows the ionization injection process. Here the peak of the injection pulse with \( a_1 = 0.15 \) is located at the optimal injection wake phase in the second bucket of the wakefield, where \( H_s - H_i \) has a maximum value. According to the trapping condition, the electrons ionized at this wake phase are above the wake seperatrix and are trapped. During the injection process, the amplitude of the wakefield is 24 GV/m, and the beam loading effect is not observed due to the low injected electron number. After the injection pulse propagates through the krypton gas, all the 9th electrons of the krypton are ionized and trapped in the wake. The trapped number is \( 1.37 \times 10^5 \mu \text{m}^{-2} \), which is in good agreement with the analytical predicted trapped number \( 1.44 \times 10^5 \mu \text{m}^{-2} \) obtained from numerically integrating the tunneling ionization rate. Fig. 4(d) shows the trapped electron number decreases with the decrease of the injection pulse amplitude \( a_1 \). PIC simulations are in good agreement with the analytical calculation.

Figure 5(a) shows the distribution of the trapped electrons in the transverse and longitudinal momentum space when the pump pulse propagates a distance of 1.33 mm. The laser parameters are the same as Fig. 2. It is found that most of the electrons are ionized at the peak of the injection pulse electric field, with a zero residual transverse momentum and that some electrons are born off-peak with a finite residual transverse momentum. The maximum of the momentum is \( p_x/m_e c = 0.115 \), which is approximately equal to the vector potential amplitude \( a_1 \). The rms transverse momentum of the electrons is \( \sigma_{p_x}/(m_e c) = 0.035 \), which is approximately equal to 0.25\( a_1 \). This residual transverse momentum contributes to the initial transverse emittance of the electron bunch. Since \( a_1 \) is an order of magnitude smaller than the vector potential amplitude used in single pulse ionization injection, the initial transverse emittance will be an order of magnitude smaller in this two-color-ionization injection scheme. Figure 5(b) shows that as the amplitude of injection pulse decreases, the rms transverse momentum of the electrons decreases; however, fewer electrons are trapped, as shown in Fig. 4(d).
Figure 4. (Color online) (a) The electric fields of the two laser pulses (black curves) and the wakefield excited by the pump pulse (red curve). (b) The electron density (black curve) and the krypton density (red curve). (c) The normalized longitudinal momenta of the electrons. (d) The trapped electron number versus the vector potential amplitude of the injection pulse. The electron density and the laser parameters are the same as Fig. 2. The krypton concentration is 1%.

Figure 5. (Color online) (a) Transverse and longitudinal momentum distribution of the trapped electrons. (b) Root-mean-square transverse momentum versus the vector potential amplitude of the injection pulse. The electron density and the laser parameters are the same as Fig. 2. The krypton concentration is 1%.
4. SUMMARY AND DISCUSSION

In this paper, we have proposed a method for generation of electron bunches with low transverse momentum by using two-color laser ionization injection. This method can produce electron beams with an order of magnitude smaller transverse momentum compared to single pulse ionization injection. Simulations using a 1D PIC code were presented that show an example where the rms residual transverse momentum of the electron beam has $\sigma_{p_x}/(m_e c) \sim 0.03$. In multi-dimensional geometry, not only the residual transverse momentum from the ionization process, but also the transverse momentum determined by the transverse force of the wakefield, transverse ponderomotive force of the laser and transverse bunch size will contribute to the transverse emittance. The transverse emittance can be estimated as $\epsilon_n \simeq \sigma_x \sigma_{p_x}/(m_e c)$ and the bunch radius can be estimated as $\sigma_x \sim w_1$, where $w_1$ is the spot size of the injection pulse. By tightly focusing the injection pulse to several $\mu m$, the estimated transverse emittance can be $< 0.1 \text{ mm mrad}$, which is an order of magnitude smaller than that in single pulse ionization injection.

5. ACKNOWLEDGMENTS

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