INFERNO: Galactic winds in dwarf galaxies with star-by-star simulations including runaway stars

Eric P. Andersson$^{1,2,\ast}$, Oscar Agertz$^2$, Florent Renaud$^2$ and Romain Teyssier$^3$

$^1$Department of Astrophysics, American Museum of Natural History, 200 Central Park West, New York, NY 10024, USA
$^2$Department of Astronomy and Theoretical Physics, Lund Observatory, Box 43, SE-221 00 Lund, Sweden
$^3$Department of Astrophysical Sciences, Princeton University, Princeton, NJ 08544, USA

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ABSTRACT
The formation and evolution of galaxies have proved sensitive to the inclusion of stellar feedback, which is therefore crucial to any successful galaxy model. We present INFERNO, a new model for hydrodynamic simulations of galaxies, which incorporates resolved stellar objects with star-by-star calculations of when and where the injection of enriched material, momentum, and energy takes place. INFERNO treats early stellar kinematics to include phenomena such as walkaway and runaway stars. We employ this innovative model on simulations of a dwarf galaxy and demonstrate that our physically motivated stellar feedback model can drive vigorous galactic winds. This is quantified by mass and metal loading factors in the range of $10 - 100$, and an energy loading factor close to unity. Outflows are established close to the disc, are highly multi-phase, spanning almost 8 orders of magnitude in temperature, and with a clear dichotomy between mass ejected in cold, slow-moving ($T \leq 5 \times 10^4 \text{ K}, v < 100 \text{ km s}^{-1}$) gas and energy ejected in hot, fast-moving ($T > 10^8 \text{ K}, v > 100 \text{ km s}^{-1}$) gas. In contrast to massive disc galaxies, we find a surprisingly weak impact of the early stellar kinematics, with runaway stars having little to no effect on our results, despite exploding in diffuse gas outside the dense star-forming gas, as well as outside the galactic disc entirely. We demonstrate that this weak impact in dwarf galaxies stems from a combination of strong feedback and a porous interstellar medium, which obscure any unique signatures that runaway stars provide.

Key words: methods: numerical – galaxies: evolution – ISM: jets and outflows

1 INTRODUCTION
Galactic evolution is governed by a manifold of connected processes over a vast range of physical scales. An important aspect of this evolution and an example of this scale-coupling is galactic scale winds driven by feedback processes in the interstellar medium (ISM). This generates a baryon cycle (for a review, see Veilleux et al. 2005; Zhang 2018). Understanding the injection of energy and momentum on parsec scales (McKee & Ostriker 1977; Katz 1992; Kim & Ostriker 2015), how this translates into outflows (Schroetter et al. 2016; Chisholm et al. 2017; Fielding et al. 2017), and how the ejected material evolves after leaving the galaxy (Tumlinson et al. 2017; Fielding et al. 2020) are fundamental questions for galaxy theory. To tackle these questions, semi-analytical models (e.g., Baugh 2006; Benson 2010), large-scale cosmological simulations (e.g., Schaye et al. 2015; Vogelsberger et al. 2014; Nelson et al. 2019), and simulations of the ISM (e.g., Walch et al. 2015; Kim et al. 2020a,b) have been employed. Progress made towards answering these questions can be attributed both to advances in numerical methods and modeling, as well as an improved understanding of the physics involved (see Somerville & Davé 2015, for a review). The complex physics of gaseous material innate to these problems make hydrodynamic simulations combined with sub-grid models for the relevant unresolved physics highly suitable for this task (see, e.g., Wheeler et al. 2019; Agertz et al. 2020; Smith et al. 2021). The recent progress made with these kinds of models has in part been facilitated by galaxy-scale simulations reaching a higher resolution, thereby better resolving processes within the ISM (and consequently the star-forming clouds), while capturing the global dynamics of evolving galaxies.

Today, galaxy simulations routinely reach a parsec-scale resolution, with star-particles representing individual stars (see, e.g., Hu et al. 2016; Emerick et al. 2018; Andersson et al. 2020, 2021; Hirai et al. 2021; Gutcke et al. 2021; Hislop et al. 2022), and in fact, should be done in this way to avoid the many restrictions (e.g., location of individual stars) imposed by the traditional approach$^1$. Star-by-star models allow for a detailed account of when and where individual stars inject momentum, energy, and enriched material. The locality of supernovae (SNe) has already been shown to affect the efficiency of stellar feedback (e.g., Walch et al. 2015; Girichidis et al. 2016; Gatto et al. 2017), in turn altering the properties of massive galaxies (e.g., Ceverino & Klypin 2009; Kimm & Cen 2014; Andersson et al. 2020) and dwarf galaxies (e.g., Gutcke et al. 2022; Steinwandel et al. 2022).

$^1$ To relieve the computational cost of tracking the vast number of stars hosted by galaxies, stars are typically modeled as single stellar populations which are tracked by a single particle. This approach becomes less sensible when the mass of the star particles is smaller than that of individual stars, which is often the case in highly resolved simulations.
et al. 2022). This indicates that star-by-star models are necessary to fully study cloud evolution, star formation, stellar feedback, chemical mixing, and thus galaxy evolution as a whole.

To this end, we present the Individual stars with Feedback, Enrichment, and Realistic Natal Motions (INFERNO) model, a new versatile star-by-star model implemented in the N-body+hydrodynamics code RAMSES (Teyssier 2002). The INFERNO model is a step towards a complete account of the physics that drives galaxy formation and evolution. In its current state, INFERNO accounts for feedback processes from giant branch stars, the rapidly evolving O and B type stars, core-collapse supernovae (CCSNe), and type Ia supernovae (SNeIa). Furthermore, INFERNO treats the early collisional dynamics in natal star clusters, which is one origin of walkaway and runaway stars (Poveda et al. 1967; Oh & Kroupa 2016).

How massive runaway stars affect galaxy evolution is still a debated question (for a review, see Naab & Ostriker 2017). These types of fast-moving stars are key examples of processes that relocate SNe. As mentioned before, this affects the stellar feedback and as a result outflows. This, often called random versus peak driving, has been explained by the interplay between clustered star formation (and consequently clustered feedback of short-lived stars, see e.g., Mac Low & McCray 1988; Nath & Shchekinov 2013; Sharma et al. 2014; Keller et al. 2014, 2016; Gentry et al. 2017, 2019), and more isolated SNe (Tang et al. 2009), as well as CCSNe with progenitors being fast-moving runaway stars (see e.g., Ceverino & Klypin 2009; Kimm & Cen 2014; Andersson et al. 2020). Nonetheless, uncertainties regarding the fraction of runaway stars (Stone 1991; Silva & Napiwotzki 2011; Eldridge et al. 2011; Maíz Apellániz et al. 2018; Renzo et al. 2019; Drew et al. 2021) make their contribution to isolated SNe an unsolved problem. Furthermore, simulations with an explicit treatment of runaway stars find contradicting results. Andersson et al. (2020) found that runaway stars exploding in low-density gas located in the inter-arm regions of large spiral galaxies result in increased outflow rates. In the dwarf galaxy simulations presented in Steinwandel et al. (2022), runaway stars were found to escape the disc of the galaxy, providing thermal energy directly to gas in the circumgalactic medium (CGM). While both these works found runaway stars to play an important role in the galactic scale outflows, Kim & Ostriker (2018) found runaway stars to have negligible effects on these outflows in simulations of stratified kpc-sized patches of the ISM (see also Kim et al. 2020a). Because of significant model variation (e.g. environment, runaway star model, and numerical scheme), no consensus is yet reached for the effect that runaway stars have on feedback physics.

One aim of this work is to study the role that the natal kinematics of individual stars (including walkaway and runaway stars) have on dwarf galaxies, in particular, the role played by the fraction of runaway stars. Dwarf galaxies are both common in the Universe (Sawala et al. 2015; Read et al. 2017; Behroozi et al. 2019), and they exhibit strong winds relative to their star formation rates (Chisholm et al. 2017; McQuinn et al. 2019). Furthermore, galactic outflows driven by strong feedback are a necessary component in the A-cold dark matter cosmological model to explain the faint-end of the galaxy-luminosity function (Dekel & Silk 1986; Benson et al. 2003), and the cored density profiles observed in many dwarf galaxies (Moore 1994; Teyssier et al. 2013; Read et al. 2016). Their low escape velocities and relatively large gas contents make them sensitive probes of stellar feedback physics (Rosdahl et al. 2015; Hu et al. 2017; Emerick et al. 2018; Su et al. 2018; Hu 2019; Smith et al. 2019; Wheeler et al. 2019; Agertz et al. 2020; Smith et al. 2021), the stellar initial mass function (IMF) (Smith 2021; Prgomet et al. 2022), and cosmic rays (Dashyan & Dubois 2020; Farcy et al. 2022; Girichidis et al. 2022). As numerical laboratories, the small sizes of dwarf galaxies make them less computationally expensive compared to Milky-Way-sized objects, therefore allowing for a large number of simulations at high numerical resolution. In the case of this work, it enables us to run a suite of simulations with a varying fraction of runaway stars, while achieving a resolution high enough to capture important aspects of stellar feedback (e.g. the Sedov-Taylor evolution of SNe, see more details in Section 3).

Our paper describes our star-by-star model INFERNO, as well as presents the theoretical work that motivations our model in Section 2, details the numerical set-up and initial conditions (ICs) in Section 3, and presents the results in Section 4. We discuss our results and place our work in a wider context in Section 5, and finally summarize and conclude in Section 6.

2 THE INFERNO MODEL

2.1 Star formation, IMF sampling & initial kinematics

Following Andersson et al. (2020, 2021), our model incorporates particles representing individual stars to follow stellar motions and feedback for stars above a mass threshold. The threshold is set by a parameter $m_\star$, and its value determines whether the feedback is calculated for individual stars, or taken as an average over the stellar population below $m_\star$. Note that $m_\star$ can take any value within a given IMF, and while small values employ a more detailed stellar model, it increases the computational cost. Using any predefined IMF, individual stars are stochastically sampled from mass $M_d$ (set as a user-defined parameter; see details in next paragraph). Star formation ensues in each cell with cold ($T < 10^4$ K) and dense ($\rho_g > 500$ cm$^{-3}$) gas. At each fine time step, several $M_d$ units of mass can be spawned through a Poisson sampling of a Schmidt-like star formation law,

$$\dot{\rho}_d = \epsilon_{ff} \frac{\rho_g}{t_{ff}},$$

where $\epsilon_{ff} = 0.1$ is the star formation efficiency per free-fall time, and $t_{ff} = \sqrt{3\pi/32G\rho_g}$ is the local gas free-fall time. In the Milky Way, the star formation efficiency per free-fall time is observed at ~ 1% with a large spread (see, e.g., Krumholz & Tan 2007; Lee et al. 2016; Chevance et al. 2022). Nonetheless, Grisdale et al. (2017) showed that on pc-scales, a larger value (~ 10%) results in a better match between simulations and observations (see also Grisdale et al. 2018, 2019). We note that the choice of $\epsilon_{ff}$ can affect the properties of the ISM and the outflows, in particular, if set too low (Hu et al. 2022). Note that in small enough cells, there is not necessarily enough mass $M_d$ to sample individual stars when the density reaches the density threshold for star formation. In such cases, star formation is delayed until enough mass is available. The population of stars with mass ($m < m_\star$) is traced by one star-particle per star formation event, and can inject feedback based on the model from Agertz et al. (2013). In this work, we keep $m_\star$ small enough (2 M$_\odot$), such that in practice this model is never applied, i.e. stars in this mass range never enter a stellar evolution phase with mass, momentum, or energy ejection.

To sample individual stars from stellar ensembles, we employ the method by Sormani et al. (2017), in which the IMF is sampled in predefined mass bins. A detailed description of our implementation can also be found in Andersson et al. (2020, see also Sormani et al. 2017). In short, the number of stars in a given stellar mass bin is determined by random number generation from a Poisson distribution with appropriate pre-computed weights. To avoid oversampling, the available mass is sampled consecutively from low to high mass,
stopping the process when the available mass is reached\(^2\). To minimize this problem we choose the mass of stellar ensembles to be \(M_\text{ej} = 500 \, M_\odot\), ensuring a well-sampled IMF (Smith 2021). For this work we use the IMF from Kroupa (2001), defined as a split power-law function \(\xi \propto m^{-\alpha_1}\) with two different mass ranges; \(\alpha_1 = 1.3\) for masses \(0.08 \sim 0.5 \, M_\odot\), and \(\alpha_2 = 2.3\) for masses \(0.5 \sim 100 \, M_\odot\).

At birth, all stellar particles receive the velocity of the gas from which they formed. For individual stars, we give the particles an additional radial velocity with isotropic distribution to model the dynamics which are unresolved in our collisionless simulations. We include two models for this: 1) stars from the same stellar ensemble receive an innate velocity dispersion \(\sigma_v\), using random sampling from a Gaussian distribution (referred to as \(\text{stir}\)); 2) velocity kicks to simulate walkaway and runaway stars\(^3\), which overrides the velocity from \(\text{stir}\) (referred to as \(\text{kick}\)). The \(\text{stir}\) model is applied to avoid stars formed at a single instance to remain perfectly overlapping. We emphasize that the \(\text{stir}\) model does not entail an accurate treatment of the collisional dynamics on small scales, which are affected by gravitational softening. The \(\text{kick}\) model, applied to a fraction \(f_{\text{kick}}\) of the massive (> 8 \, M_\odot), unless otherwise stated) stars, models walkway and runaway stars associated with early dynamical interactions in natal star clusters. For this work, we use the inverse power-law distribution \(f_v \propto v^{-1.8}\), covering the range \(3 < v < 375 \, \text{km s}^{-1}\). This is the velocity distribution of stars escaping a 10\(^{3.5}\) \, M_\odot natal cluster in its first 3 Myr of evolution, as modeled by Oh & Kroupa (2016). This is the same distribution used for massive stars (> 8 \, M_\odot) in Andersson et al. (2020), and one of two runaway star models tested by Steinwandel et al. (2022).

2.2 Stellar evolution & feedback

\textsc{INFERNO} accounts for the injection of energy, momentum, and chemically enriched material, with a model taking the initial mass, metallicity, and age of a given star into consideration. These models apply to different stellar evolutionary stages, and each is described in detail throughout this section. The main factor determining when stars move between evolutionary phases is the main-sequence lifetime. We calculate this using the fitting function from Raiteri et al. (1996) calibrated to the Padova tracks (Alongi et al. 1993; Bressan et al. 1993; Bertelli et al. 1994).

The chemical evolution of stars and gas is based on stars inheriting the chemical composition of the gas from which they form, and then injecting chemically enriched material (henceforth referred to as yields). To determine the yield of a given stellar evolution process we use bilinear interpolation of yield tables from NuGrid (Pignatari et al. 2016; Ritter et al. 2018). This set provides yields for a wide range of stellar masses and metallicities, although we note that there are other yield tables in the literature, with large differences in total yield (see Buck et al. 2021, for a comparison). This method allows us to track up to 80 of the elements in the periodic table, which we describe in more detail in Andersson et al. (in preparation). The stellar evolution models depend only on the total stellar metal mass which we approximate as \(M_2 = 2.09M_\odot + 1.06M_\text{Fe}\), based on Solar mixture (Asplund et al. 2009).

Similarly to the yields, all mass loss is computed by interpolating the NuGrid tables. Figure 1 shows the total mass lost through different feedback channels as a function of the initial mass of a given star. Note that we ensure that the mass expelled by a given star can never result in particles with a negative mass.

2.2.1 Winds from massive O & B stars

The most massive stars (> 8 \, M_\odot) have high enough luminosity to push away material from their surface during the main-sequence phase of their evolution. During this phase, stars launch a fast (~ 1000 \, km s\(^{-1}\)) stellar wind. This wind is driven by the extreme stellar radiation, pushing on the stellar envelope through resonant line absorption (Vink 2015). Due to its early onset after the formation of a star, this wind can aid the disruption of star-forming clouds, suppresses star formation locally, and affects the clustering of stars (see e.g., Dale & Bonnell 2008; Rosen et al. 2014; Lancaster et al. 2021).

Our model assumes that all stars in the mass range \(8 \sim 60 \, M_\odot\) launch a wind at a constant velocity of 1000 \, km s\(^{-1}\), for the entire duration of the main sequence. Depending on the stellar mass, the mass loss rates range from \(10^{-8} \sim 10^{-6} \, M_\odot\, \text{yr}^{-1}\). As shown in Figure 1, the mass-loss-rate increases non-linearly with stellar mass.

\(^2\) This model sometimes suffers from under-sampling the most massive stars, which affects the stellar feedback budget. However, the steepness of the IMF makes this under-sampling rare (handful of times per Gyr).

\(^3\) Walkaways as stars are typically referred to as stars with peculiar velocities \(v < 30 \, \text{km s}^{-1}\), while runaways have \(v > 30 \, \text{km s}^{-1}\). We use this convention in our work. These stars originate from either the internal dynamics of star clusters (Poveda et al. 1967) or via binary system breakup due to instantaneous mass loss from companion SNe (Blaauw 1961). Both these scenarios favor more massive stars becoming runaways. The former is due to mass segregation, moving massive stars to the dense center of the cluster, and the latter is due to binary fraction increasing with stellar mass. The kick distribution we apply to escaping stars was estimated from numerical simulations of the first 3 Myr of the cluster’s evolution (see Oh & Kroupa 2016, for details). This does not account for the SNe break-up of binary systems, which is constrained by the time of the first SNe (\(\geq 3\) Myr). The velocity distribution used for escapers results in 86% walkaways and 14% runaways.

\(^4\) We note that this mass range does not include all B-type stars. For lower mass stars (< 8 \, M_\odot) of this class, we refer to Section 2.2.3 for details about wind treatment.
making extrapolation above the NuGrid upper mass limit (25 M\(_\odot\)) sometimes exceeding the initial stellar mass. To avoid this, we assume a constant mass-loss rate for all stars more massive than this limit. This implies that our model likely underestimates the amount of momentum and energy from these winds, although we note that typical IMFs make stars with mass > 25 M\(_\odot\) rare.

### 2.2.2 Core-collapse supernovae

CCSNe result in the instantaneous release of ~ 10\(^{51}\) erg of energy, making them a crucial component of any stellar feedback model (McKee & Ostriker 1977; Katz 1992; Kimm et al. 2015). The explosion is triggered at the end of the main sequence for massive stars (> 8 M\(_\odot\)), however, the exact mechanism behind the explosion is not fully understood\(^5\). This uncertainty is the often-called islands of explodability (Janka 2012; Zapartas et al. 2021), stating that many models favor specific ranges in stellar mass to trigger an explosion, with the alternative being the direct collapse to a compact object. Typically, the most massive stars go through the direct collapse channel, however, extremely massive stars (> 100 M\(_\odot\)) can undergo pair-instability explosions resulting in the complete disruption of the star (see e.g. Fryer et al. 2001).

Keeping the above complexity in mind, our model assumes that all stars in the mass range 8 – 30 M\(_\odot\) undergo CCSNe after leaving the main sequence, instantaneously depositing 10\(^{51}\) erg of energy, along with chemically enriched material, into its immediate surroundings. The mass expelled during the CCSNe event is shown by the red line in Figure 1. For stellar masses above this range, we assume that leaving the main sequence results in direct collapse into a black hole, without any injection of energy or enriched material. This implies that the earliest possible injection of energy via SNe occurs 6 Myr after star formation (see Figure 2).

### 2.2.3 Stellar winds from giant stars

Stars more massive than 0.5 M\(_\odot\) enter a giant phase for a short period after leaving the main sequence unless the star undergoes SNe before this. In this phase, energy is mostly generated through hot-bottom burning in convective shells exterior to the stellar core, periodically supplying the core with fuel giving rise to explosive burning (see Höfner & Olofsson 2018, for a review). These surges in energy (often called thermal pulses) drive a stellar wind with mass loss rates in the range 10\(^{-8}\) – 10\(^{-4}\) M\(_\odot\) yr\(^{-1}\) at velocities \(\approx 10\) km s\(^{-1}\) (see e.g. Schöier & Olofsson 2001; Olofsson et al. 2002; González Delgado et al. 2003; Ramstedt et al. 2009; Eriksson et al. 2014). Although this wind makes up only a small fraction of the stellar feedback energy budget, it is crucial for the chemical enrichment of the ISM. A source of uncertainty in stellar evolution models with regards to giant stars is the intermediate phase (7.5 – 9 M\(_\odot\)) between evolving into a white dwarf or CCSNe (Poelarends et al. 2008; Doherty et al. 2017). After leaving the main sequence, these stars are massive enough to ignite carbon burning in their core, resulting in a large number of thermal pulses giving rise to a super asymptotic giant branch phase. During this phase, material fueled to the core can result in its mass exceeding the Chandrasekhar mass, leading to the core explosion.

Our model assumes that all stars in the mass range 0.5 – 8 M\(_\odot\) enter a post-main-sequence phase, during which a stellar wind is expelled. The wind is injected as a source of momentum at a constant mass loss rate of 10\(^{-5}\) M\(_\odot\) yr\(^{-1}\) with a velocity of 10 km s\(^{-1}\). The duration of this phase is set by the total mass lost (green line in Figure 1), computed from the NuGrid tables, i.e. winds are expelled until no more mass is available, in which case the star is considered to have become a white dwarf. The resulting initial-final mass relation roughly matches that in Cummings et al. (2016).

### 2.2.4 Type Ia supernovae

SNeIa are essential for the chemical evolution of galaxies as they are a source of Fe-peak elements, with some contribution to α (see e.g., Seitenzahl et al. 2013; Kobayashi et al. 2020). Although their origin is still not fully understood, mass transfer to a degeneracy-supported object in a binary system seems ubiquitous to models, with a near-Chandrasekhar-mass white dwarf primary being the most favorable candidate (Bloom et al. 2012). Due to their uncertain origins, empirical models assuming delay-time distributions weighted by cosmic star formation histories are often used for modeling SNeIa rates (see e.g., Mannucci et al. 2006; Maoz et al. 2014; Maoz & Graur 2017).

Our model incorporates the field normalized delay-time distributions from Maoz & Graur (2017), giving a SNeIa rate per unit mass

\[ n_{\text{Ia}} = n_{\text{Ia}} \left( \frac{t}{\text{Gyr}} \right)^{-1.12} \Delta t, \quad t > t_{\text{Ia}}, \]

assuming a delay time \(t_{\text{Ia}} = 38\) Myr (main sequence lifetime of 8 M\(_\odot\) star), and normalization \(n_{\text{Ia}} = 2.6 \times 10^{-13} \text{ yr}^{-1} \text{ M}_\odot^{-1}\). Because of the uncertainty regarding progenitor\(^6\), as well as a missing tracer for bi-

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\(^5\) The currently favored hypothesis is delayed neutrino-heating, which ejects the outer layers of the stars (see Janka 2012, for a review).

\(^6\) Note that these rates do not assume a progenitor, however, our chemical yield model does. SNeIa yields from Seitenzahl et al. (2013) assumes a Chandrasekhar-mass delayed-detonation scenario.
nary stars in our model, we use the particles tracing the unresolved stellar component to determine possible locations of SNeIa. To compute the number of SNeIa, each star particle representing unresolved stars stores the total mass of coeval stars and uses it to normalize $n_{\text{Ia}}$ for a given star particle age. This number ($\ll 1$) is used to determine the probability of an event, ultimately sampling discrete SNIa. Each explosion releases $10^{51}$ erg of energy and 1.4 $M_{\odot}$ of mass into its immediate surrounding.

Figure 2 summarizes the feedback budget of our model, showing the cumulative mass, momentum, and energy which is injected into the surroundings of a $10^5 M_{\odot}$ mono-age population of stars over 1 Gyr. With the exception of winds from OB-type stars, the onset of feedback from the different sources is determined by the main-sequence lifetime of the most massive star in the relevant population of stars. The range of timescales for this onset highlights the importance of including a multitude of feedback sources, as this affects both how star formation proceeds locally, and shapes the environment for subsequent feedback.

3 NUMERICAL SETUP AND MODEL IMPLEMENTATION

INFERNO is implemented in the adaptive-mesh-refinement (AMR) and $N$-body code RAMSES (Teyssier 2002). RAMSES evolves the gas by solving the fluid equations on a refinement grid with a second-order unsplitted Godunov method, assuming an ideal mono-atomic gas with an adiabatic index of 5/3. The cooling module applied combines equilibrium thermochemistry of hydrogen and helium (Court & Alimi 2004; Rosdahl et al. 2013), metal line cooling rates computed with CLOUDY (Ferland et al. 1998), and a uniform UV background (Haardt & Madau 1996) including an on-the-fly self-shielding model (Aubert & Teyssier 2010; Rosdahl & Blaizot 2012). The equilibrium chemistry of hydrogen and helium considers photoionization, collisional ionization and excitation, recombination, free-free emission, Compton cooling and heating, and dielectronic recombination. For a more detailed discussion, see Rey et al. (2020). We limit gas cooling down to a minimum temperature of 1 K. The dynamics of stars and dark matter are tracked using collisionless particles, whose contribution to the gravitational potential is added to the AMR grid with the cloud-in-cell particle-mesh method. The forces are calculated by solving the Poisson equation with a multi-grid method (Guillet & Teyssier 2011). A quasi-Lagrangian refinement strategy ensures roughly 8 particles in each cell, which reduces discreteness effects (Romeo et al. 2008). Furthermore, cells are split into 8 new cells, using a refinement mass criterion of $8 \times 100 M_{\odot}$. We limit cell-splitting to 16 levels of refinement, providing a spatial resolution limit of ~1.5 pc for our simulations, which are set up in a box with 100 kpc side length. Figure 3 highlight the frequency of cells at the different resolution (refinement levels) in a phase diagram ($\rho$ versus $T$) taken as a representative simulation output. We do not consider the Jeans criterion in our refinement strategy. Hopkins et al. (2018) showed that the ISM is primarily supported by turbulence rather than thermal pressure, even down to cloud scales. This fact alleviates the resolution requirement set by, e.g., Truelove et al. (1997) (note that the red line in Figure 3 shows the density and temperature at which the thermal Jeans length is equal to our smallest cell size). Thus we argue that the effective Jeans length (thermal plus turbulent) is likely resolved in our simulations, with cold gas at high densities being treated by the star formation recipe (see also discussion in van Donkelaar et al. 2022).

We employ INFERNO on a dwarf galaxy to study how efficiently stellar feedback drives outflows. The simulated galaxy is an analog of the Wolf–Lundmark–Melotte (WLM) galaxy with a gas mass $M_{\text{gas,disc}} \approx 7 \times 10^7 M_{\odot}$, an initial stellar disc with mass $M_{\text{S,disc}} = 10^7 M_{\odot}$ and a dark matter halo with mass $M_{\text{DM}} = 10^{10} M_{\odot}$. The latter two are comprised of 12.5 $M_{\odot}$ stellar particles and 1650 $M_{\odot}$ dark matter particles. We consider the initial stellar component only as a mass component (i.e. with no contribution to feedback or enrichment).

The ICs were almost identical to those in Smith et al. (2021). The ICs comprised of gas and stars, has an exponential radial density profile with a scale length of 1.1 kpc. The vertical gas distribution is set in accordance with hydrostatic equilibrium at an initial temperature of $10^4$ K, while the vertical distribution of stars is initialized with a Gaussian distribution with a scale height of 0.7 kpc. Initially, the gas disc has a metallicity of 0.1 $Z_{\odot}$. The dark matter profile matches an NFW profile (Navarro et al. 1996) with a spin parameter $\lambda = 0.04$ and concentration parameter $c = 15$. The ICs were generated using MakeDiscGalaxy (Springel 2005) and mounted onto the AMR grid using the cloud-in-cell method. These generated ICs do not fill the full extent of our simulated box, hence cells without out assigned properties are initialized with a density of $10^{-5}$ cm$^{-3}$, a metallicity of 0.001 $Z_{\odot}$, and a temperature of $3 \times 10^4$ K. These ICs are almost identical to those in Smith et al. (2021).

Since we do not consider feedback processes from the stars included in the ICs, the initial gas support is purely thermal. This energy support is quickly radiated away resulting in a sudden collapse and star formation burst, which is typical for galaxies simulated in isolated boxes. To mitigate this effect we start the simulation without gas cooling and then ramp it up exponentially (formally we scale the internal energy sink responsible for cooling by $(t/t_0)^5$, effectively re-scaling the cooling rate) over the first $t_0 = 100$ Myr. This method allows for a calm initialization of the galaxy. We do not include this transient in any of our result figures.

The stellar feedback model injects energy, momentum, and chemically enriched material at each fine time step (i.e. between the time integration of each refinement level). Every timestep we loop through all stars and inject the relevant feedback quantities into the oct closest to the star particle (8 neighboring cells), updating the density, veloc-
ity, and pressure of each cell. Momentum is added isotropically. If a star enters a new evolutionary stage during a timestep (which affects the feedback model), we adapt the calculation to only cover the part of the timestep during which stellar feedback is active. Furthermore, two safety criteria (a maximum advection velocity of 6000 km s\(^{-1}\), and a maximum temperature of 10\(^{9}\) K) are employed to ensure the stability of the hydrodynamics solver.

Because the resolution is limited (specifically in low-density gas by the AMR prescription) the momentum buildup in the quasi-energy-conserving stage of SNe explosions is not always captured. To handle this problem, we first calculate the radius \(r_{ST}\) of the blast-wave when it transitions from energy conserving to momentum conserving (i.e., from the Sedov-Taylor phase to the often called snowplow phase, Sedov 1959; Taylor 1950). If this radius is not resolved by at least 6 cells we inject the terminal momentum \(p_{ST}\) that would have built up during the energy conserving stage. We compute the cooling radius from \(r_{ST} = 30 \frac{E_{51}}{\rho_{g}^{7/17}} \frac{Z_{g}^{1/17}}{\rho_{g}^{7/17}}\) pc, where \(E_{51}\) is energy in units of \(10^{51}\) erg, \(\rho_{g}\) is cell density in units cm\(^{-3}\), and \(Z_{g}\) is metallicity in solar value. This follows from the analytical blast-wave solution (Blondin et al. 1998), to which we have added a metallicity scaling calibrated to our cooling function (Thornton et al. 1998). Similarly, the terminal momentum is calculated from \(p_{ST} = 2.95 \times 10^{2} \frac{E_{16}^{1/17}}{\rho_{g}^{2/17}} \frac{Z_{g}^{2/17}}{\rho_{g}^{2/17}}\) M\(_{\odot}\) km s\(^{-1}\), where we have adjusted the scaling following Kim & Ostriker (2015). Based on the blast wave criterion, roughly 5% of SNe are unresolved in our simulations. In recent work, Hu (2019) suggests that the injection of momentum does not accurately capture the evolution of a SNe. Although unexplored for the type of code employed here, we caution the reader that 5% of our SNe might underestimate the amount of energy incorporated into the ISM. We leave a detailed exploration of this for future work, but see Appendix B.

Figure 4. Projected gas density of the simulations studied in this work, shown in face-on projection on the top row and edge-on projection on the bottom. The snapshots shown are at \(t = 400\) Myr, and all snapshots for a given simulation in the time-span 300 – 500 Myr are similar, with the exception of transient events, such as super-bubble outbreaks.

Figure 5. Star formation rate as a function of time for our simulations, computed by summing the stellar mass in 10 Myr age bins. The dashed horizontal line shows the observed star formation rate of WLM (Karachentsev et al. 2013). With the inclusion of stellar feedback, star formation is significantly reduced as a result of the loss of cold gas.

4 RESULTS
As detailed in Section 1, the aims of this work are (i) verifying that INFERNO produces realistic ISM conditions for galaxy evolution, (ii) exploring the physics of outflows in a dwarf galaxy, and (iii) investigating how these outflows are affected by natal stellar kinematics. For the latter, we compare the results of 8 dwarf galaxy simulations with identical ICs, but with different natal velocity distributions. In addition, a ninth simulation (no feedback) serves as an example of not including stellar feedback. To maintain clarity, the main body of this work includes the detailed analysis of 4 simulations: 1) no feedback, with no energy or momentum injection from stellar feedback sources; 2) \(\sigma_v = 0\), with neither stir or kick applied; 3) \(\sigma_v = 0.01\) km s\(^{-1}\), with stir applied; 4) \(f_{kick} = 0.2\), with \(\sigma_v = 0.01\) km s\(^{-1}\) stir and
Figure 6. Pressure at different gas densities in the disc of our simulations (denoted by the title of each panel). These quantities are measured in each cell for all outputs and plotted as time-averaged (300 – 500 Myr), mass-weighted 2D-histogram. The dotted lines show temperatures $10^9$, $10^9$, $10^9$, and $10^8$ K from the bottom right to the top left, computed from the ideal gas law.

Figure 7. Probability distribution of gas density, showing volume (mass) weighted distributions for $f_{\text{kick}} = 0.2$ in the filled grey histogram (thick black line), and colored lines (different models labeled in legend) showing the distribution of densities where CCSNe exploded. Note that all models with feedback have similar volume and mass-weighted distributions. All results are taken as time averages for the final 200 Myr of each run. The top inset shows the ratio of the distributions between the two models including natal stellar velocities (distinguished by the same color as in the bottom plot) and the $\sigma_v = 0$ model.

Figure 4). For feedback applied. The full suite of simulations are shown in Appendix A, where we divided them into stir models ($f_{\text{kick}} = 0$), and kick models ($f_{\text{kick}} > 0$). The no feedback simulation has a $\sigma_v = 0.01$ km s$^{-1}$ stir applied. The choice of $f_{\text{kick}} = 0.2$ is motivated by the cluster escape fractions ranging from 10 to 30% for massive stars, as found in Oh & Kroupa (2016). After the initial relaxation (200 Myr) we follow the evolution for 500 Myr, covering a few orbital times. Our analysis only concerns the final 500 Myr of evolution.

4.1 Effect on interstellar medium

With the exception of no feedback, the visual appearances of the gas properties in our simulations are similar (see e.g., gas density in Figure 4). For no feedback, the absence of energy and momentum sources results in a cold and fragmented disc. In contrast, the inclusion of stellar feedback significantly reduces the number of clouds and creates hot low-density voids in between the gaseous spiral structure. Furthermore, feedback drives gas out of the galaxy, generating a complex gas structure above and below the disc. This inner circum-galactic medium (CGM) is similar in all feedback models, regardless of the natal kick model. This is unlike those found in Steinwandel et al. (2022), as well as results for more massive systems, which have been shown to be strongly affected by the inclusion of runaway stars (Ceverino & Klypin 2009; Andersson et al. 2020, but see Kim & Ostriker 2018; Kim et al. 2020a). We discuss this further in Section 5.

Feedback leads to a lower star formation rate (SFR), quantified in Figure 5. At early times ($t < 200$ Myr), the lack of significant inflows causes the gas content to reduce over time, with an accompanying decrease in SFR in all simulations. For simulations including feedback, the SFR flattens after this period, as fountain flows are starting to regulate the supply of gas to the galaxy. In the first 300 Myr of these simulations, the total gas mass fraction $f_g = M_g/(M_g + M_*$) is reduced by $\approx 10\%$, while that of only cold ($T < 10^4$ K) gas is reduced by $\approx 20\%$. From this, it is clear that feedback reduces the amount of gas available for star formation, in part due to outflows which we focus on in Section 4.2. In the simulations including feedback, the SFR is compatible with that observed in the WLM galaxy ($\sim 6 \times 10^{-3} M_\odot$ yr$^{-1}$, Karachentsev et al. 2013) at $\approx 200$ Myr. The galaxies evolve with periodic variations in the SFR, on average lying below the observed rate by a factor of few after 200 Myr. The periodicity arise from bursts in stellar feedback act in response to the periods of high star formation. For example, in the case of $\sigma_v = 0.01$ km s$^{-1}$, a complete shutdown of SFR occurs between 430 and 470 Myr.

In addition to suppressing the SFR, stellar feedback generates an over-pressured hot phase in the ISM and large low-density bubbles. Figure 6 shows this highly multi-phase gas structure of the disc (defined as a cylinder with a radius of 3.5 kpc and height of 1 kpc, as outlined with red lines in the right plots of Figure 8). The pressure $P$ of simulations including feedback spans several orders of magnitude ($P/k_B \sim 1 - 10^9$ K cm$^{-3}$ at $\rho = 1$ cm$^{-3}$, where $k_B$ is the Boltzmann constant). The majority of high-pressure gas is generated by clustered feedback and the natal stellar velocity model plays only a minor role. The clustered nature stems from vigorous star formation in dense clouds and proceeds until halted by the onset of the first CCSNe (6 Myr). Before this disruption of the star-forming clouds, the gas collapse is suppressed by stellar winds.
Figure 7 compares the average probability density function (PDF) of the gas densities for the simulations. For a given coeval stellar population, the first CCSNe typically explode in dense gas ($\rho \sim 10^4$ cm$^{-3}$), rapidly building up a low-density bubble ($10^{-6} < \rho < 10^{-3}$ cm$^{-3}$) for subsequent CCSNe. During the buildup of the bubble, CCSNe explode in intermediate gas densities ($10^{-2} \leq \rho \leq 10^2$ cm$^{-3}$). In the top panel, we show the ratio between the explosion densities of the two simulations including natal kinematic models and the $\sigma_0 = 0$ model. Surprisingly, $\sigma_0 = 0.01$ km s$^{-1}$ deviates the most from $\sigma_0 = 0$ (clearly visible at $\rho = 10^{-5}$ cm$^{-3}$), although the difference is small and subject to stochasticity between measurements. The minor role of runaway stars in determining the explosion density distribution is due to their rarity in comparison to non-runaway stars. For our galaxy, the effect that stellar feedback has on the gas dynamics is completely dominated by the clustered CCSNe. This is apparent in the outflows, which we explore in the following section.

4.2 Outflows and inner CGM

The energy supplied by our feedback model translates into a galactic wind, resulting in large amounts of gas being pushed out of the galaxy. Significant amounts of gas return in galaxy scale fountain flows, while the rest is accelerated to outflow velocities $v_{\text{out}}$ exceeding the escape velocity $v_{\text{esc}}$ (described in more detail in Section 4.3). Here we explore the interplay between the outflowing gas and the inner parts of the CGM, focusing on the final 200 Myr of the simulations. We no longer consider any results from the no feedback model, due to its inability to generate outflows.

We measure the properties of outflowing gas at two interfaces located outside the galaxy. Their location (white filled) and extent (white dotted) are displayed on top of projected density maps of the $f_{\text{kick}} = 0.2$ simulation in Figure 8. We refer to the interface located close to the disc as “launching,” and the spherical shell interface, which encapsulates the inner CGM, as “inner-outer halo.” Note that these definitions vary in the literature, and that outflow properties can depend on how these are defined. We measure the properties of the outflowing gas by summing a quantity $q_i$ multiplied by the gas velocity $v_i$, considering only cells with outward moving gas within a given region.\footnote{Variables indexed by $i$ refer to their value in individual cells. For the launching interface, this is formally calculated following}

$$\frac{dq_z}{dz} = 1 \sum_i q_i |v_z,i|, \quad \text{for} \quad \begin{cases} v_z,i > 0, & \text{if } z_i > 0 \\ v_z,i < 0, & \text{if } z_i < 0 \end{cases}$$

where the sum runs over cells ($i$) in a cylindrical slab with thickness $\Delta z = 0.1$ kpc placed $\pm 1$ kpc from the disc mid-plane. For the inner-outer halo interface, we use

$$\frac{dq_r}{dr} = 1 \sum_i q_i |v_r,i|, \quad \text{for} \quad v_r,i = v_i \cdot \hat{r} > 0$$

where the sum runs over cells in a spherical shell with a radius of 9 kpc (roughly equal to 20% of the virial radius) and a thickness $\Delta r = 2$ kpc. The coordinate system has its origin at the center of the galaxy and its directions are indicated in the density maps to the right in Figure 8. In Equation 4, $v_i$ is the velocity vector, and $\hat{r}$ is the radial unit vector.

The top left plot in Figure 8 shows the mass outflow rate as a function of time\footnote{There is some ambiguity in how one defines the vertical outflows, and in our case, we chose to compute the outflows in the two slabs independently and then sum them. For modeling purposes, the total outflow through both slabs is most useful, as it captures the mass loss from the disc. Observationally, the outflow measurements are typically limited to a single cone and then multiplied by a factor of two (assuming symmetry), in order to capture the total outflow rate (see, e.g., Schroetter et al. 2019). We find little to no difference between the two slabs, justifying this assumption.}. The remaining three left plots show the time evolution of the logarithm of mass, metal, and energy loading factors, which we define as

$$\eta_M = \frac{M_g}{SFR}, \quad \eta_Z = \frac{Z_g}{\xi g \cdot SFR}, \quad \eta_E = \frac{E_{\xi SN}}{\xi g \cdot SFR}$$

respectively, where $Z_g$ is the gas metallicity of the disc, and $\xi SN = 4.89 \times 10^5$ km$^2$ s$^{-2}$ is the average energy injected by CCSNe from stellar populations with a fully sampled Kroupa (2001) IMF assuming $10^{51}$ erg per CCSNe (c.f., Kim & Ostriker 2017; Smith et al. 2021).

The gas mass ejected in outflows exceeds the mass consumed in star formation by up to two orders of magnitude. This is the case for all three models, which all show outflow rates of similar average values. Furthermore, the values are similar both at the launching and the inner-outer halo interfaces. As noted in the previous paragraph, wind properties are in general sensitive to where they are measured and here their similar values are coincidental, as the vertical placement of the launching interface affects the value measured. Surprisingly, this is not the case for the inner-outer halo which we discuss in more detail in Section 4.3.

The mass loading factor increases in the first 200 Myr, and then reach values that fluctuate between $\sim 10 \sim 1000$, independently of the natal stellar velocity model. This is also the case for the metal loading factor, although its value slightly exceeds $\eta_M$. The energy loading factors do not show an initial increase but display similar fluctuations around the same time. As with the other loading factors, these fluctuations grow significantly stronger at later times, resulting in values of $\eta_E$ in the range $\sim 0.1 \sim 100$. These fluctuations are the result of variations in SFR, and the outflow properties remain more stable (see e.g. mass outflow rate in the top left plot of Figure 8).

In a broader context, high mass loading factor ($10 \sim 100$) for low mass galaxies are typically required by semi-analytical models (see e.g., Benson et al. 2003; Somerville & Davé 2015) and large volume simulations to match observed galaxy scaling relations (e.g., Mitchell et al. 2020). Metal loading factors are typically found to be of the same order or in excess of the mass loading factor (Yates et al. 2021), as we also find here. INFERNO captures these heavily mass and metal-loaded winds without fine-tuning any feedback parameters. Comparisons of energy loading factors are more difficult since these depend strongly on the details of the feedback model, as well as the cooling and structure of the CGM. In our case, the absence of a cosmological environment, and $\eta_{E}$ around unity gives rise to a CGM with total energy set by the stellar feedback budget. Compared to studies of outflows with similar feedback model and galaxy (e.g., Smith et al. 2021; Steinwandel et al. 2022) our values of $\eta_E$ are high, which we discuss further in Section 5.1. Our loading factors roughly match those in observed galaxies (Chisholm et al. 2017, 2018), although it should be noted that completeness issues and differences in the geometrical definition of where outflows are measured make loading factors notoriously difficult to estimate, in particular for dwarf galaxies (see Collins & Read 2022, for a review). For mass and energy loading, Chisholm et al. (2017) accounts only
for the photo-ionized gas, which does not necessarily capture the entire outflow (a notion returned to later). Furthermore, because of the strong temporal fluctuations we find in our simulation, a better comparison would be to investigate if the range of loading factors in our simulations matches the scatter in observations. However, such a comparison would necessitate more observational data points for the galaxy mass range we consider.

4.3 Time-averaged wind properties

We now turn to time-averaged properties of the outflows, considering only the final 200 Myr of each simulation. Note that for loading factors (see Equation 5) we consider the fraction of the mean of the numerator and denominator separately, rather than the mean of the loading factor itself. This alleviates the problem of ill-defined loading factors when the denominator is zero. Furthermore, we do...
not account for the scatter in SFR, but only consider that of the outflow. A similar approach is sometimes used in the literature when quoting loading factors resolved in time (see e.g., Hislop et al. 2022; Steinwandel et al. 2022).

Figure 9 shows the average loading factors as a function of vertical distance (left) and radius (right). In addition to mass, metal, and energy loading factors we also include momentum loading factor\(^9\), as well as the energy loading factor split into thermal and kinetic energy. As previously mentioned, we see that while the vertical profile decreases with distance, the radial remains roughly constant. The decrease in vertical loading factors comes from the cylindrical slabs with a constant radius being unable to capture the full extent of the conical outflow, as these slabs are moved out. The outflow transition from thermally dominated to kinetically dominated around \(z = 3\) kpc in all simulations. This is not only the result of gas cooling but also gas acceleration (seen as an increase in momentum loading). The acceleration arises due to pressure gradients existing in the halo, shown in Figure 10. We compute this by taking the gradient of the pressure profile and subtracting the gravitational force from the NFW profile (Navarro et al. 1996, the disc has negligible contribution to the potential outside 2 kpc). We find that the acceleration becomes positive around 2 kpc, and flattens at a value of \(1 \text{ km s}^{-1} \text{ Myr}^{-1}\) around 3 kpc. The flattening coincides with the transition between thermally and kinetically dominated gas energy. Provided that the acceleration can proceed far out in the halo, it can accelerate gas to \(100 \text{ km s}^{-1}\) in 100 Myr. As already indicated by the similarity in mass outflow rate (Figure 8), there is little difference between the models. Furthermore, this affects the velocity structure of the gas between the \textit{launching} and \textit{inner-outer halo} interfaces, described below.

Figure 11 shows the velocity and temperature structure of the outflows. The figure is divided into two sets of subplots, the two rows on top show the \textit{launching} interface, while the two bottom rows show the \textit{inner-outer halo} interface. In the \textit{launching} interface, we find that outflows with temperature \(T \lesssim 5 \times 10^4\) K dominate the mass budget (first row), while hotter outflows dominate the energy budget (second row). The majority of the mass resides in gas with velocities up to \(100 \text{ km s}^{-1}\). Above \(100 \text{ km s}^{-1}\), the temperature of the gas increases along a trend of roughly constant Mach number \(M = 1.0\). This increase roughly coincides with the escape velocity of the dark matter halo. For the \textit{launching} interface, this trend only includes a small fraction of mass. At the peak of the trend, we find most of the energy, at temperatures around \(\sim 10^8\) K and velocities \(\gtrsim 1000 \text{ km s}^{-1}\). This is in broad agreement with Kim et al. (2020b), who find a similar dichotomy in cold and hot gas when comparing the mass and energy budget of these different phases (see also Rathjen et al. 2022).

When the gas reaches the \textit{inner-outer halo}, more mass has been entrained into the fast and hot phase of the wind. We also find that the energy transitions toward more kinetic (the transition is indicated by the filled red line in Figure 11), likely driven by gas thermalization. The trend along a constant Mach number appears clearly, in particular in energy-weighted velocity-temperature space. As in the \textit{launching} interface, the gas is limited to subsonic velocities.

Finally, we summarize the mass, metal, and energy loading factor for all simulations in Figure 12, including those presented in Appendix A. The mass and energy loading factors of all our simulations are compared to the values from empirically derived fitting functions by Chisholm et al. (2017), shown with black dashed lines. A similar fitting function for metal loading factor is presented in Chisholm et al. (2018), however, our values underestimate these by 2 orders of magnitude, hence we omit including these estimates on the linear vertical axis of Figure 12. We do not find large differences among our simulations, but rather that all simulations have \(\eta_M \sim 5 \sim 40\), \(\eta_Z \sim 10 \sim 60\), and \(\eta_E \sim 0 \sim 2\). The largest value and scatter are found in \(\sigma_v = 1 \text{ km s}^{-1}\), and in \(f_{\text{kick}} = 0.5\) when including walkaway and runaway stars. The minor role of runaway stars is likely a result of highly porous ISM, as well as a halo that is highly energetic. We discuss this and other factors which might affect the small role of runaway stars in Section 5.2.

5 DISCUSSION

The results covered have been focused on the \textsc{infernno} model’s ability to regulate star formation and drive galactic scale outflows via stellar feedback. For a dwarf galaxy, our model generates a strong steady outflow, with large (> 10) mass and metal loading factors, as well as the energy loading factor close to unity (summarised in Figure 12). When resolved in time, we find that the loading factors display strong fluctuations (two orders of magnitude) as a result of bursty SFR. High loading factors on the dwarf mass scale are necessary to reproduce the faint end of the galaxy mass function (Naab & Ostriker 2017), a notion that is also supported empirically (Chisholm et al. 2017, 2018; Schroetter et al. 2019). The outflows are more metal-rich compared to the ISM, however, not to the extent found by Chisholm et al. (2018). We investigate this further in Andersson et al. (in preparation), where we present the full chemical evolution model implemented in \textsc{infernno}. Our outflows are highly multi-phase in nature, covering a large range of temperatures. This is crucial for the degree of ionization in the CGM (Tumlinson et al. 2017). In stark contrast to previous results obtained for massive disc galaxies (Andersson et al. 2020), we find that the natal velocity distribution of the stars plays a minor role in setting the loading factor on dwarf scales. In the following sections, we discuss this in more detail.

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\(^9\) Momentum loading factor is measured by dividing \(\rho\) (computed from Equations 3 & 4, with \(q_i = m_i v_i\)) by the product of star formation rate and \(1.25 \times 10^3/95.5 \text{ km s}^{-1}\). See Kim et al. (2020b) for details on the normalization.
Figure 11. Temperature-velocity diagrams for outflowing gas shown for the launching (inner-outer halo) interface in the top (bottom) two rows. We weigh the maps by mass or specific energy, as indicated by the color bar on the right-hand side of each row. Each panel shows the time average of the 2D-histograms for all outputs in the last 200 Myr. Each column shows the simulation indicated by the column title. The dotted black lines draw order of magnitude Mach numbers \( M = \frac{v_{\text{out}}}{c_s} \) calculated from the sound speed of ionized gas \( c_s^2 = \frac{k_B T}{\mu m_{\text{H}}} \) with \( \mu = 1/2 \). Solid red lines indicate where the kinetic \( 0.5v^2 \) and thermal \( 2P/\rho \) energy of the outflowing gas is equivalent. The red dashed line shows the escape velocity of the dark matter halo at the location of the interface.

5.1 Comparisons with contemporary feedback models

Our simulation setup of a dwarf galaxy in an isolated environment allows us to reach parsec scale resolution, which is comparable to works by e.g. Hu (2019); Emerick et al. (2020); Smith et al. (2021); Steinwandel et al. (2022). While the initial gas mass of these models varies (particularly in Emerick et al., who simulated an ultra-faint dwarf), the mass and metal loading factor are in broad agreement. However, the energy loading factor of our simulations is around unity, while the aforementioned works routinely find values around 0.1. As discussed below, this discrepancy by an order of magnitude could provide insight into differences in feedback models and numerical treatment. The energy supplied to the halo affects the re-accretion of material, dividing feedback into preventive (inhibiting gas inflow) and ejective (expelling gas) feedback (Davé et al. 2012). For a thorough literature comparison, we refer to Li & Bryan (2020).

Of particular interest is the work by Smith et al. (2021, see also Smith 2021). Smith et al. investigated a suite of simulations with similar ICs and numerical resolution, but with a different hydrodynamics solver, star formation recipe, and for a range of different feedback sources (see also Hu 2019). The SN-PE model in Smith et al. is the most comparable in terms of included feedback processes (although we include SNIa and stellar winds, which may be of importance, see Section 5.2.2), with which we find slightly lower mass loading (factor
Figure 12. Mean and standard deviation of mass (top), metal (center), and energy (bottom) loading factors taken over the last 200 Myr of all our simulations. Red markers show the loading factors as measured at the launching interface, while blue points show that measured at the inner-outer halo interface. Note that all models including a fraction of stars with the walkaway and runaway velocity distribution (\(f_{\text{kick}} \neq 0\)) also impose the \(c_r = 0.01 \text{ km s}^{-1}\) distribution on stars that are not kicked. The black dashed line (errors indicated by gray region) shows the value from the empirical fitting function of Chisholm et al. (2017).

2), but a significantly higher energy loading (factor 10). Note that when Smith et al. introduces radiation feedback, the energy loading decreases significantly, thereby increasing the discrepancy with our model. The origin of the discrepancy between our model and that of Smith et al. is not clear; however, Hu et al. (2022) found notable decreases significantly, thereby increasing the discrepancy with our model. Concerning energy injection, RAMSES updates the energy in a fixed volume (set by the refinement level), while (quasi-) Lagrangian codes (e.g., Hu 2019; Smith et al. 2021, the latter using the moving-mesh method of AREPO) often update energy in regions of fixed mass. This difference may affect the injection feedback, e.g., adiabatic cooling processes or spatial clustering of injection events. Likely, the numerical method plays other roles as well, a factor which has been discussed extensively in literature (see, e.g., Kim et al. 2014, 2016; Roca-Fàbrega et al. 2020; Hu et al. 2022). Further efforts to understand the differences between codes (particularly for star-by-star models) are likely necessary to reach a consensus.

5.2 The weak impact of natal stellar kinematics on stellar feedback

5.2.1 The role of disc structure and the ISM

As previously mentioned, the density structure of the ISM likely plays a role in how relevant runaway stars are. In Andersson et al. (2020), the inclusion of runaway stars resulted in a supply of CCSNe progenitors into large under-dense regions which enabled SNe to more efficiently drive outflows (Ohlin et al. 2019). This could also explain the disagreement found by Kim et al. (2020b), which does not capture the low-density regions imparted by spiral arm shearing and the full geometrical extent of the galaxy (see also Martizzi et al. 2016). In the simulations presented here, the low SFR implies that the number of runaway stars is low; hence, although low-density regions develop, they are unlikely to receive a significant number of runaway stars before dissolving. We confirmed this through a visual inspection of our simulations.

Furthermore, the shallow potential of the disc in the dwarf galaxy implies a thick gas disc (initial scale height \(h_{\text{disc}} = 0.7 \text{ kpc}\)). As such, stars need to travel a long distance to reach dramatically different environments, even when traveling vertically (unless reaching far out in the CGM, see Section 5.2.3). In contrast, runaway stars in more massive disc galaxies (e.g. as in Andersson et al. 2020 with a gas disc scale height of \(h_{\text{disc}} = 0.34 \text{ kpc}\)) have a shorter travel distance to environments with as dramatic differences (e.g. in gas density).

The weak impact of runaway stars could be connected to the star formation threshold (500 cm\(^{-3}\)). Such a high density implies that star formation depletes the local gas reservoir on a timescale \(\tau_{\text{dep}} = \rho_g/\dot{\rho}_{\text{sf}} = t_{\text{ff}}/\epsilon_{\text{ff}} \approx 20 \text{ Myr}\), which is similar to the timescale for SNe. Varying the star formation threshold and \(\epsilon_{\text{ff}}\) affects the clustering of SNe and to some extent the outflow properties (Smith et al. 2021). If gas is depleted fast, massive stars in clusters explode as SNe in low-density gas, leading to efficient heating of the ISM (e.g., Agertz & Kravtsov 2015). Differences in star formation recipes (as well as numerical resolution, see discussion in Kim et al. 2020a) could be the cause for the discrepancy in the results of, e.g., this work, Kim & Ostriker (2018), Andersson et al. (2020), and Steinwandel et al. (2022). This would explain the lack of consensus regarding the impact of runaway stars. However, the full explanation is likely more intricate, with many factors playing a role, e.g. overall structure of...
The different red lines show SNeIa rates for different models widely used in weighted density distribution for the Figure 6, the filled grey histogram (thick black line) shows the volume (mass) densities where SNeIa explodes in our simulations. As in Figure 13, assuming a simple toy model with exponential SFR = \exp(-t/5 \text{ Gyr}) M_{\odot} \text{ yr}^{-1}. Also shown is the number CCSNe associated with runaway stars for different values of $f_{\text{kick}}$, as well as several different models for the SNIa rate. In our simulations, we adopt the model by Maoz & Graur (2017). The second model shown is from Graur et al. (2014), which is the same as Maoz & Graur (2017) but normalized to fit data from galaxy clusters (half the rate of field galaxies). The model by Raiteri et al. (1996) has been widely used in early galaxy models (see e.g., Greggio & Renzini 1983; Matteucci & Greggio 1986; Agertz et al. 2013). We also show the model derived by Mannucci et al. (2006) used in the FIRE2 model for galaxy simulations (Hopkins et al. 2014, 2018; Gandhi et al. 2022).

The SNIa rate builds up in the first few Gyr, and is comparable to the number of SNe associated with runaway stars even in models assuming a high fraction of kicked stars ($f_{\text{kick}} \geq 0.5$). To our best knowledge, the role that this build-up of SNeIa has on non-cosmological simulations is not well explored in the literature.

We show the gas densities where SNeIa explodes in Figure 14. Interestingly, we find that the density distribution of SNeIa explosions is a combination of the mass- and volume-weighted density PDF. If distributed homogeneously, one expects this distribution to follow the volume-weighted one. Nonetheless, we find the Ia explosions to extend toward higher densities. Furthermore, we find no correlation between the age of the star particle when the Ia occurs and the explosion density, implying that even early Ia is no longer associated with any particular density.

If SNeIa affects the role of runaway stars, this might explain some of the discrepancies between our results and those of e.g. Smith et al. (2021); Steinwandel et al. (2022).

5.2.3 CGM and out-of-disc runaway stars

Steinwandel et al. (2022) finds that out-of-disc runaway stars can supply a significant amount of energy, thereby increasing the energy loading in simulations that include runaway stars. We do not find this to be the case in our simulations, despite us studying a galaxy of similar mass, and we see runaway stars escaping into the halo (see Figure A3). It is likely that the high energy loading of all our simulations creates an environment around the galaxy that makes additional thermal energy dumps negligible. Indeed, in the case of $f_{\text{kick}} = 0.2$, the CGM inside the inner-outter halo interface contains $\sim 400 \times 10^{54}$ erg of thermal energy throughout its later evolution, i.e. hundred times larger than what any single SNe would provide. Compared to this highly energy-loaded halo, out-of-disc runaway stars only supply a small amount of energy (we find only $\sim 40$ SNe 200 pc above the disc in the final 200 Myr of our $f_{\text{kick}} = 0.2$ simulation).

Another aspect of such a high thermal energy content is that this establishes a negative pressure gradient. As shown in Section 4.3, this results in an outward acceleration of significant amounts of gas ejected from the galaxy. Furthermore, it is likely that material is accelerated to high velocities by SNe blast waves ($1000 \text{ km s}^{-1}$) that break out from the disc. The details of this will be explored in future work.

5.2.2 The role of type Ia supernovae

A key aspect of the supposed effect that massive runaway stars have on stellar feedback is that they explode far away from where they were formed. This leads to more randomly distributed SNe sites, in contrast to SNe only around star-forming gas (see, e.g., Li et al. 2015, 2017). To a large extent, this is also the case for delayed SNe, e.g. SNeIa with rates which are a few tens of per cent of the CCSNe (Tammann et al. 1994). Exploring the role of these SNe in the context of dwarf galaxies warrants follow-up work, but we can speculate on their effect since our model implements a method to include these objects. Note that at late times in our simulations (final 200 Myr), SNeIa makes up $\sim 20\%$ of the total SNe population. With only a small per cent of stars being runaways, SNeIa may in fact be the main contributor to randomly located stellar explosions. To exemplify this for an extended star formation history, we show the number of CCSNe and SNeIa in Figure 13, assuming a simple toy model with exponential SFR = \exp(-t/5 \text{ Gyr}) M_{\odot} \text{ yr}^{-1}. Also shown is the number CCSNe associated with runaway stars for different values of $f_{\text{kick}}$, as well as several different models for the SNIa rate. In our simulations, we adopt the model by Maoz & Graur (2017). The second model shown is from Graur et al. (2014), which is the same as Maoz & Graur (2017) but normalized to fit data from galaxy clusters (half the rate of field galaxies). The model by Raiteri et al. (1996) has been widely used in early galaxy models (see e.g., Greggio & Renzini 1983; Matteucci & Greggio 1986; Agertz et al. 2013). We also show the model derived by Mannucci et al. (2006) used in the FIRE2 model for galaxy simulations (Hopkins et al. 2014, 2018; Gandhi et al. 2022).

The SNIa rate builds up in the first few Gyr, and is comparable to the number of SNe associated with runaway stars even in models assuming a high fraction of kicked stars ($f_{\text{kick}} \geq 0.5$). To our best knowledge, the role that this build-up of SNeIa has on non-cosmological simulations is not well explored in the literature.

We show the gas densities where SNeIa explodes in Figure 14. Interestingly, we find that the density distribution of SNeIa explosions is a combination of the mass- and volume-weighted density PDF. If distributed homogeneously, one expects this distribution to follow the volume-weighted one. Nonetheless, we find the Ia explosions to extend toward higher densities. Furthermore, we find no correlation between the age of the star particle when the Ia occurs and the explosion density, implying that even early Ia is no longer associated with any particular density.

If SNeIa affects the role of runaway stars, this might explain some of the discrepancies between our results and those of e.g. Smith et al. (2021); Steinwandel et al. (2022).
5.3 Limitations of INFERNO

This article presents the first iteration of the INFERNO model. Therefore the model has several remaining limitations. This section highlights the most prominent of these limitations.

With the ability to reduce the clustering of star formation (see, e.g., Hislop et al. 2022), radiation feedback typically limits loading factors, particularly in energy (Smith et al. 2021). Furthermore, Agertz et al. (2020) showed that radiative feedback strongly affects the formation of ultra-faint dwarf galaxies (by significantly suppressing star formation, radiation leads to an overall calmer evolution). INFERNO does not yet include radiation feedback, although stellar winds play a similar (but weaker) role (Andersson et al., in preparation). Radiative hydrodynamics are already implemented in RAMSES-wr (Rosdahl et al. 2013, 2015). This model is currently being adapted for INFERNO and will account for radiation feedback using stellar spectra from individual stars to employ star-by-star radiation feedback. How this affects runaway stars remains unclear.

The star formation recipe employed by INFERNO relies on IMF sampling from discrete quanta of stellar material $M_d$. To ensure accurate sampling, $M_d$ is constrained by $\geq 500 M_{\odot}$ (see, e.g., Smith 2021). This mass constraint implies that an increasing resolution forces higher gas density to allow star formation. How this affects the formation of stars in our simulations is not clear. Solutions to this problem are to either abandon predefined mass bins for IMF sampling and immediately sample stars from the IMF (see, e.g., Lahén et al. 2019) or to introduce sink particles to model the star formation process at scales smaller than the resolution elements (see, e.g., Bate et al. 1995; Klessen et al. 2016; Gatto et al. 2017). An advantage of introducing sink particles is that this allows a more straightforward way to model time-resolved star formation (e.g., the delayed formation of massive stars Haugholle et al. 2018) and time-dependent natal velocity kicks (see, e.g., Oh & Kroupa 2016).

Because collisional gravitational dynamics are far from resolved in our simulations, our model is not predictive concerning the physics of binary stars. The sub-grid model for runaway stars and SNe type Ia only depends on binary objects implicitly. Furthermore, stellar multiples are necessary to explain exotic astrophysical objects, such as stripped envelop stars, SNe kicks, and stellar mass transfer (see, e.g., Hurley et al. 2002; Izzard et al. 2006). These aspects affect, e.g., stellar feedback, chemical enrichment, and stellar kinematics, and are therefore of interest to investigate further in INFERNO. In the context of stellar multiplicity, Blaauw kicks (Blaauw 1961) are particularly interesting for our model since these are a source of runaway stars. Blaauw kicks are triggered by immediate mass loss in a binary system when the companion star undergoes SNe (note that this implies a time delay before the velocity kick). Our model does not include this effect because the velocity distribution applied only accounts for the first 3 Myr star cluster evolution (Oh & Kroupa 2016). Be mindful that our model adds all velocity kicks at the birth of each stellar population. Introducing binary stars via a parametrized method could allow us to explore these aforementioned physical processes without the necessity of costly collisional dynamics (see, e.g., Eldridge et al. 2011; Kim & Ostriker 2017).

Finally, INFERNO remains limited by an equilibrium cooling physics (see, e.g., Katz et al. 2022, for details on the effects of non-equilibrium chemistry) and lacks several physical mechanisms known to affect galaxy evolution (e.g., magnetic fields and cosmic rays, see Naab & Ostriker 2017). For example, cosmic rays can generate a pressure gradient that drives primarily cold and warm gas into the outflows (see, e.g., Rathjen et al. 2022), which would appear as an additional phase at a lower temperature in Figure 11. Future efforts toward making INFERNO a more detailed model for galaxy simulations will focus on these aspects.

6 SUMMARY & CONCLUSIONS

We present a new galaxy physics model called INFERNO, introducing a star-by-star treatment for the injection of momentum, energy, and chemically enriched material, each with timing, locality, and amount calculated based on the properties of individual stars. We employ INFERNO to simulate the evolution of a dwarf galaxy to study how stellar feedback drives outflows. Our results focus on the mass, metal, and energy loading factors, as well as the properties of galactic winds.

We draw the following concluding remarks from our study:

(i) Our stellar feedback model causes a lowering of star formation by roughly two orders of magnitude while driving strong gas outflows. A galactic wind is established close to the disc (around $\pm 2$ kpc from the disc mid-plane) and moves material through the CGM. We recover mass and metal loading factors on the order of $10^{-100}$, as required to match the faint end of the galaxy mass function (Naab & Ostriker 2017). Furthermore, the wind is heavily energy-loaded, with an energy loading factor close to unity.

(ii) The galactic winds display a clear dichotomy in the mass and energy outflow, with mass primarily carried by cold gas ($T \approx 10^5$ K) at velocities $v < 100$ km s$^{-1}$, while energy is carried in a hot ($T > 10^7$ K), fast ($v > 100$ km s$^{-1}$) wind. The energy evolves with distance from the galaxy, transitioning from thermally dominated to kinetically dominated a few kpc above the disc plane. Our model generates a highly energetic CGM where outflows are limited to the subsonic regime, with high-velocity gas ($v > 100$ km s$^{-1}$) following a trend of roughly constant Mach number $M \sim 0.1$ in the velocity-temperature space.

(iii) We find no strong effects imposed by the different natal velocity distribution applied to newly formed stars. While we include runaway stars in our model, we find a surprising insensitivity to their presence, in stark contrast to more massive galaxies where runaway stars play a significant role in setting the outflows (Andersson et al. 2020). Not only is this the case for outflows ejected by dwarfs, but we find similar SFRs, gas multi-phase structures, and SNe explosion densities, regardless of what natal stellar velocity distribution we apply.

The precise role played by runaway stars for galaxy evolution is not yet established, with varying conclusions in the literature (Ceverino & Klypin 2009; Kimm & Cen 2014; Andersson et al. 2020; Kim et al. 2020b; Steinwandel et al. 2022). At this stage, the literature covers a wide range of galaxy masses, which are simulated with a multitude of different models. This work is the first in a series that will employ INFERNO, with the aim of exploring runaway stars, as well as galaxy evolution physics in general.

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DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the corresponding author.

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In this appendix, we address how sensitive our results are to the resolution of our simulations. Selecting the $f_{\text{kick}}$ effectively reduces the fraction of collisions between particles, and thus the fraction of co-natal stars that escape clusters through dynamical interactions (Oh & Kroupa 2016). Because both the fraction of stars born in clusters and the fraction of stars which escape clusters is not well known, we parameterize this with a kick fraction $f_{\text{kick}}$ and apply it only to massive stars ($> 8 \, M_\odot$). We tested values 0.01, 0.1, 0.2, 0.5 and 1.0. Note that for $f_{\text{kick}} = 1.0$ the fraction of massive runaway stars is 14%. We find little to no effect from runaway stars for all values, as shown in A2.

Finally, in Figure A3 we show the locations of recent CCSNe for all models with the face-on view in the upper plot and edge-on view in the lower plot. This is shown on top of the temperature maps of all models with the face-on view in the upper plot and edge-on view in the lower plot. This is shown on top of the temperature maps of all models with the face-on view in the upper plot and edge-on view in the lower plot.

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Finally, in Figure A3 we show the locations of recent CCSNe for all models with the face-on view in the upper plot and edge-on view in the lower plot. This is shown on top of the temperature maps of each simulation. Notably, we see how the number of out-of-disc SNe increases, as we increase $f_{\text{kick}}$.

**APPENDIX B: RESOLUTION TESTS**

In this appendix, we address how sensitive our results are to the resolution of our simulations. Selecting the $f_{\text{kick}} = 0.2$ model, we re-
simulate the evolution of the galaxy at lower resolution to see whether significant differences appear in the outflow rates and loading factors. The resolution of the simulations can be affected either by limiting the maximum level of refinement or by changing the mass criterion for when refinement is triggered. To investigate the sensitivity to both these refinement criteria, we simulated one galaxy with a maximum refinement level at 13 levels (i.e., at three levels lower, resulting in a max spatial resolution of 12 pc) and one where the refinement mass increased by a factor 10 (i.e., a refinement mass of \(8 \times 10^3 \, M_\odot\)). Note that decreasing the numerical resolution affects the highest densities (due to the smoothing of gravitational forces). Since the star formation recipe operates at the resolution limit, the star formation threshold must be adapted to provide a similar star formation history. There is no straightforward method for this. However, through tests, we find that changing the star formation threshold to 10 cm\(^{-3}\) in the case when the spatial resolution is limited to 12 pc and 50 cm\(^{-3}\) for a refinement mass of \(8 \times 10^3 \, M_\odot\) provides star formation rates that are similar to the simulations at the original simulations (we also present results from simulations where the star formation threshold remained unchanged).

In Figure B1, we show the star formation rate, outflow rate, and loading factors as a function of time for the simulations at different resolutions. Note that at early times, not adapting the star formation threshold results in a slower build-up of the star formation rate and, consequently, the outflow rate. Nonetheless, the loading factors are less affected by this, indicating that the energy and momentum budget of the feedback model remains similar. Note that in the case of 12 pc (\(8 \times 10^3 \, M_\odot\), roughly 10% (15%) of SNe have unresolved Sedov-Taylor evolution). At later times, the wind displays similar rates in all simulations.

While the changes to the resolution in the most highly resolved parts of the galaxy (e.g., the ISM) do not drastically affect our results, this is not necessarily the case for the CGM. As shown in Rey et al. (2023), increasing the resolution outside the galaxy (which is inherently low due to the nature of the AMR) can significantly boost the outflow rates. How strongly this affects the results presented here and in all other work focusing on outflows remains to be seen.

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Figure A3. Gas temperature in slices through the centre of our simulation boxes showing the face-on view in the top panels and edge-on view in the bottom panels. All plots shown are for $t = 400$ Myr, and the panels have a width of 8 kpc. Each panel shows a different simulation denoted by the label in the upper left corner. The location of recent (≲ 5 Myr in the disc; ≲ 50 Myr outside the disc) SNe are shown in white points.
Figure B1. Star formation rate, outflow rate, mass, metal, and energy loading shown from top to bottom as a function of time for the $f_{\text{kick}} = 0.2$ simulation at a different resolution. The green, thick line shows the results presented in the main body of the article (spatial resolution of ~1.5 pc, and mass resolution of 100 $M_\odot$). The thin lines show simulations at lower resolution (12 pc in blue and 1000 $M_\odot$ in orange). The star formation density threshold is $10$ cm$^{-3}$ and $50$ cm$^{-3}$ in 12 pc and 1000 $M_\odot$, respectively (see main text for details). The dotted lines show simulations with a star formation density threshold identical to the original simulations ($500$ cm$^{-3}$).