Hadronic resonances enhanced by thresholds

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(Dated: Version of November 13, 2017)

Abstract

We present a neat example of a meson–baryon system where the vicinity of two different thresholds enhances the binding of a hadronic resonance, a pentaquark. As a consequence the pattern of states may change when moving among different flavor sectors, what poses a warning on naive extrapolations to heavy flavor sectors based on systematic expansions. For this purpose we simultaneously analyze the $N\bar{D}$ and $NB$ two-hadron systems looking for possible bound states or resonances. When a resonance is controlled by a coupled-channel effect, going to a different flavor sector may enhance or diminish the binding. This effect may, for example, generate significant differences between the charmonium and bottomonium spectra above open-flavor thresholds or pentaquark states in the open-charm and open-bottom sectors.

PACS numbers: 14.40.Lb,12.39.Pn,12.40.-y

Keywords:
The interpretation of the recently discovered baryonic states at the LHCb, $P_c(4380)^+$ and $P_c(4450)^+$, as well as some of the exotic mesonic states discovered in the hidden-charm or hidden-beauty sector is still puzzling \[2, 3\]. A common feature of all these states seems to be the proximity of their masses to two-hadron thresholds. Their naive description as simple baryon-meson or meson-meson resonances gave rise to predictions of bound states in heavier flavor sectors by different spectroscopic models, like those based on the traditional meson theory of the nuclear forces or resorting to heavy quark symmetry arguments \[4, 5\].

In a recent paper \[6\] a mechanism to explain the stability or metastability of the exotic mesonic states discovered in the hidden-charm or hidden-beauty sector was proposed. It was pointed out how two effects have to come together to allow for the formation of a bound state above open-flavor thresholds: the presence of two nearby thresholds and a strong coupling between them, in spite of the fact that the diagonal interactions contributing to this state are not strong. Thus, such mechanism, as long as it is possible avoids the risk of proliferation of states appearing in some quark-model calculations.

For the $X(3872)$ this is well plausible \[7\]. It was pointed out that two of the possible dissociation thresholds are almost exactly degenerate, the one corresponding to spin-singlet charmed meson plus a spin-triplet anti-charmed meson (or conjugate), and the one made of a light vector-meson and a charmonium vector-meson. For instance, in the flavor-$SU(3)$ limit, the $H$ dibaryon benefits of the degeneracy of the $\Lambda\Lambda$ and $N\Sigma$ thresholds, and is found stable in some model calculations, whereas for broken $SU(3)$ the degeneracy is lost and the $H$ dibaryon becomes unstable in the same models \[8\].

This idea had been already anticipated in a qualitative analysis of the possible dissociation thresholds of four-quark systems with a $Q\bar{Q}n\bar{n}$ structure (in the following $n$ stands for a light quark and $Q$ for a heavy $c$ or $b$ quark), making stringent predictions as the non-existence of a bottom partner for the $X(3872)$ or the existence of exotic doubly heavy mesons \[9\]. While the first prediction seems to survive experiment in contrast to those of other theoretical models \[4, 5\], the second is still awaiting for an experimental effort \[10\]. We wonder if there could be a neat example where one could think of some degeneracy of two baryon-meson thresholds leading to exotic or crypto-exotic baryons, as it may be the case for some of the exotic meson states \[9\]. The existence of an exotic state in a given flavor sector can not be naively generalized to other flavor sectors in case of loss of the vicinity of the thresholds. In a similar manner, its non-existence in a particular flavor sector does not exclude its presence.
in different flavor sectors.

In this letter we discuss a relevant example of a five-quark state in the $NB$ two-hadron system that clearly exemplifies the importance of the mechanism we have previously presented. It should be considered in the phenomenological analysis of the recently reported pentaquark states and may serve as a guideline for the study of the pattern of exotic states in the baryon and meson sectors \[2\]. Our findings come up in the shadow of a previous study of a different two-hadron system, $N\bar{D}$, whose generalization to the bottom case gave rise to an a priori unexpected result that remarks the effect of the almost degeneracy of two different baryon-meson thresholds.

In Ref. \[11\] we studied the $N\bar{D}$ system by means of a chiral constituent quark model. Our main motivation at that time was the study of the interaction of $D$ mesons with nucleons which is a goal of the PANDA Collaboration at the European facility FAIR \[12\]. Thus, our theoretical study was a challenge to be tested at the future experiments. In this letter we perform a parallel study of the $NB$ system (with a similar quark structure, $nnnn\bar{Q}$) looking for similarities and differences with respect to the $N\bar{D}$ system. Our objective is to highlight a particular case where the vicinity of thresholds will enhance the binding of the baryon-meson system disrupting the number and the ordering of states obtained in the charm sector. Although the conclusions of this study aim to be independent of the particular details of the interacting model used, we for instance made use of the chiral constituent quark model (CCQM) of Ref. \[13\]. It was proposed in the early 90’s in an attempt to obtain a simultaneous description of the nucleon-nucleon interaction and the baryon spectra \[14\]. It was later on generalized to all flavor sectors giving a reasonable description of the meson and baryon spectra. The model is based on the assumption that the light–quark constituent mass appears because of the spontaneous breaking of the original $SU(3)_L \otimes SU(3)_R$ chiral symmetry at some momentum scale. In this domain of momenta, quarks interact through Goldstone boson exchange potentials. QCD perturbative effects are taken into account through the one-gluon-exchange potential. Finally, it incorporates confinement as dictated by unquenched lattice QCD calculations. A detailed discussion of the model can be found in Refs. \[13, 14\].

The systems under study, $N\bar{D}$ and $NB$, do not present quark-antiquark annihilation complications that may obscure the predictions of a particular model under some non-considered dynamical effects. They contain a heavy antiquark, what makes the interaction
rather simple. The quark-model used provides parameter-free predictions for the interaction in a baryon-meson system with charm $-1$ or bottom $+1$. Besides, the existence of identical light quarks in the two hadrons generates quark-Pauli effects in some particular channels, what gives rise to an important short-range repulsion due to lacking degrees of freedom to accommodate the light quarks [14].

To study the possible existence of exotic states made of a light baryon, $N$ and $\Delta$, and a charmed meson, $\bar{D}$ and $\bar{D}^*$, or a bottom meson, $B$ and $B^*$, we solve the Lippmann-Schwinger equation for negative energies looking at the Fredholm determinant $D_F(E)$ at zero energy [15]. If there are no interactions then $D_F(0) = 1$, if the system is attractive then $D_F(0) < 1$, and if a bound state exists then $D_F(0) < 0$. This method permitted us to obtain robust predictions even for zero-energy bound states, and gave information about attractive channels that may lodge a resonance [7]. We consider a baryon-meson system $Q_iR_j$ ($Q_i = N$ or $\Delta$ and $R_j = \bar{D}$ or $\bar{D}^*$ for charm $-1$ and $R_j = B$ or $B^*$ for bottom $+1$) in a relative $S$ state interacting through a potential $V$ that contains a tensor force. Then, in general, there is a coupling to the $Q_iR_j D$ wave. Moreover, the baryon-meson system can couple to other baryon-meson states, $Q_kR_m$. We show in Table I the coupled channels in the isospin-spin $(T, J)$ basis for the $NB$ system (for the $N\bar{D}$ system one would replace $B$ by $\bar{D}$ and $B^*$ by $\bar{D}^*$). Let us briefly sketch the method to look for bound state solutions using the Fredholm determinant. If we denote the different baryon-meson systems as channel $Q_iR_j \equiv A_n$, the Lippmann-Schwinger equation for the baryon-meson scattering becomes

$$t_{\alpha \beta; TJ}^{\ell_\alpha s_\alpha, \ell_\beta s_\beta} (p_{\alpha}, p_{\beta}; E) = V_{\alpha \beta; TJ}^{\ell_\alpha s_\alpha, \ell_\beta s_\beta} (p_{\alpha}, p_{\beta}) + \sum_{\gamma=1, A_2, \cdots} \sum_{\ell_\gamma=0, 2} \int_0^\infty p_{\gamma}^2 dp_{\gamma} V_{\alpha \gamma; TJ}^{\ell_\alpha s_\alpha, \ell_\beta s_\beta} (p_{\alpha}, p_{\gamma})$$

$$\times G_{\gamma}(E; p_{\gamma}) t_{\gamma \beta; TJ}^{\ell_\gamma s_\gamma, \ell_\beta s_\beta} (p_{\gamma}, p_{\beta}; E), \quad \alpha, \beta = A_1, A_2, \cdots,$$

where $t$ is the two-body scattering amplitude, $T$, $J$, and $E$ are the isospin, total angular momentum and energy of the system, $\ell_\alpha s_\alpha$, $\ell_\beta s_\beta$, and $\ell_\gamma s_\gamma$ are the initial, intermediate, and

| TABLE I: Interacting baryon-meson channels in the isospin-spin $(T, J)$ basis. |
|---------------------------------------------------------------|
| $T = 0$  | $T = 1$  | $T = 2$  |
| $J = 1/2$ | $NB - NB^*$ | $NB - NB^* - \Delta B^*$ | $\Delta B^*$ |
| $J = 3/2$ | $NB^*$    | $NB^* - \Delta B - \Delta B^*$ | $\Delta B - \Delta B^*$ |
| $J = 5/2$ | $-$       | $\Delta B^*$                 | $\Delta B^*$ |
final orbital angular momentum and spin, respectively, and \( p_\gamma \) is the relative momentum of the two-body system \( \gamma \). The propagators \( G_\gamma(E; p_\gamma) \) are given by

\[
G_\gamma(E; p_\gamma) = \frac{2\mu_\gamma}{k_\gamma^2 - p_\gamma^2 + i\epsilon},
\]

with

\[
E = \frac{k_\gamma^2}{2\mu_\gamma},
\]

where \( \mu_\gamma \) is the reduced mass of the two-body system \( \gamma \). For bound-state problems \( E < 0 \) so that the singularity of the propagator is never touched and we can forget the \( i\epsilon \) in the denominator. If we make the change of variables

\[
p_\gamma = d \frac{1 + x_\gamma}{1 - x_\gamma},
\]

where \( d \) is a scale parameter, and the same for \( p_\alpha \) and \( p_\beta \), we can write Eq. (1) as

\[
t_{\alpha_\beta;TJ}(\ell_{\alpha_\alpha}, s_{\alpha}; x_\alpha, x_\beta; E) + \sum_{\gamma=A_1, A_2, \ldots} \sum_{\ell=0, 2} \int_{-1}^{1} d^2 \left( \frac{1 + x_\gamma}{1 - x_\gamma} \right)^2 \frac{2d}{(1 - x_\gamma)^2} dx_\gamma 
\times V_{\alpha_\gamma;TJ}(\ell_{\alpha_\gamma}, s_{\alpha}; x_\gamma, x_\beta; E) = 0.
\]

We solve this equation by replacing the integral from \(-1\) to \(1\) by a Gauss-Legendre quadrature which results in the set of linear equations

\[
\sum_{\gamma=A_1, A_2, \ldots} \sum_{\ell=0, 2} \sum_{m=1}^{N} M_{\alpha_\gamma;TJ}^{\ell_{\alpha_\alpha}, m\ell_{\gamma} s_{\gamma}}(E) t_{\ell_{\gamma} s_{\gamma}, m\ell_{\beta} s_{\beta}}(x_m, x_k; E) = V_{\alpha_\beta;TJ}(\ell_{\alpha_\beta}, s_{\alpha_\beta}; x_n, x_k),
\]

with

\[
M_{\alpha_\gamma;TJ}^{\ell_{\alpha_\alpha}, m\ell_{\gamma} s_{\gamma}}(E) = \delta_{nm}\delta_{\ell_{\alpha_\alpha}, \ell_{\gamma} s_{\gamma}} - w_m d^2 \left( \frac{1 + x_m}{1 - x_m} \right)^2 \frac{2d}{(1 - x_m)^2} 
\times V_{\alpha_\gamma;TJ}(\ell_{\alpha_\gamma}, s_{\alpha}; x_n, x_m) G_\gamma(E; p_{\gamma m}),
\]

and where \( w_m \) and \( x_m \) are the weights and abscissas of the Gauss-Legendre quadrature while \( p_{\gamma m} \) is obtained by putting \( x_\gamma = x_m \) in Eq. (4). If a bound state exists at an energy \( E_B \), the determinant of the matrix \( M_{\alpha_\gamma;TJ}(E_B) \) vanishes, i.e., \( |M_{\alpha_\gamma;TJ}(E_B)| = 0 \). We took the scale parameter \( d \) of Eq. (4) as \( d = 3 \) fm\(^{-1}\) and used a Gauss-Legendre quadrature with \( N = 20 \) points.

Using the method described above, we have solved the coupled-channel problems of the \( N\bar{D} \) and \( NB \) baryon-meson systems. The two-body interactions are obtained from the
TABLE II: Character of the interaction in the different $N\bar{D}$ $(T, J)$ states.

| $T$ = 0 | $T$ = 1 | $T$ = 2 |
|---------|---------|---------|
| $J = 1/2$ | Repulsive | Repulsive | Weakly repulsive |
| $J = 3/2$ | Weakly attractive | Weakly repulsive | Attractive |
| $J = 5/2$ | – | Attractive | Strongly repulsive |

CCQM of Refs. [13, 14] as explained in Ref. [11]. The Pauli principle at the level of quarks plays an important role in the dynamics of these baryon-meson systems, because states containing Pauli blocked channels, $(T, S) = (2, 5/2)$, or Pauli suppressed channels, $(T, J) = (0, 1/2)$ and $(T, J) = (1, 1/2)$, are repulsive, see Table III.

Let us first discuss the $N\bar{D}$ system. In Table III we summarize the character of the interaction for the different $(T, J)$ states, being the most attractive ones the $(T, J) = (2, 3/2)$ and $(T, J) = (1, 5/2)$. We show in Fig. 1 their Fredholm determinant. The state with quantum numbers $(T)J^P = (1)5/2^-$ shows a bound state with a binding energy of 3.9 MeV. It corresponds to a unique physical system, $\Delta \bar{D}^*$, that would appear in the scattering of $\bar{D}$ mesons on nucleons as a D wave resonance, what could in principle be measured at PANDA [12]. The $(T, J) = (2, 3/2)$ state contains a coupled-channel problem, $\Delta \bar{D} - \Delta \bar{D}^*$.

![Fredholm determinant](image1)

FIG. 1: $(T, J) = (2, 3/2)$ (left panel) and $(T, J) = (1, 5/2)$ (right panel) Fredholm determinant of the $N\bar{D}$ system.
While the diagonal interactions are not even attractive, the coupling between them is strong because the decay $\bar{D}^* \rightarrow \bar{D} + \pi$ is allowed, but not enough to generate a bound state as can be seen in the left panel of Fig. 1.

When the mass of the heavy meson is increased the contribution of the kinetic energy is reduced. Thus, the binding energy of the $NB$ system is expected to be slightly larger than in the $N\bar{D}$ case, because $\bar{D}$ and $B$ mesons have similar interactions with nucleons due to having the same quark structure. This is why we have repeated the calculation for the $NB$ system looking for deeper bound states in a baryon-meson system with a heavier antiquark. We depict in Fig. 2 the Fredholm determinant of the two channels that were found to be attractive in the $N\bar{D}$ system, see Table II. Surprisingly, the increment in the attraction is not regularly spread over the different $(T,J)$ channels. The $(T,J) = (1, 5/2)$ state is strongly affected and becomes the lowest one with an important gain of binding, showing a bound state with a binding energy of 42 MeV. The ordering of the attractive channels is therefore reversed with respect to the $N\bar{D}$ system as can be seen in Fig. 2.

What is the responsible for this unexpected behavior of the binding energy as the mass of the heavy meson augments? The reason lies on the internal structure of the states and the behavior of the thresholds when increasing the heavy meson mass. As mentioned above, the $(T,J) = (1, 5/2)$ state is made of a unique physical system, $\Delta \bar{D}^*$ in the charm sector.
or $\Delta B^*$ in the bottom sector, and thus there are no coupled-channel effects. Moving from the charm to the bottom sector gives rise to a small gain of binding, from 3.9 MeV in the $N\bar{D}$ system to 5.3 MeV in the $NB$ system, as one would naively have expected due to a smaller kinetic energy contribution but keeping a rather similar interaction. However, the $(T, J) = (2, 3/2)$ state contains a coupled-channel problem, $\Delta \bar{D} - \Delta \bar{D}^*$ in the charm sector and $\Delta B - \Delta B^*$ in the bottom sector. Whereas the diagonal potentials are not strong, as mentioned above, the coupling between the two channels is important because the $\bar{D}^* \to \bar{D} + \pi$ or $B^* \to B + \pi$ decays are allowed. When moving from the charm to the bottom sector the most important effect is the reduction of the mass difference between the two thresholds contributing to this state. The mass difference between vector and pseudoscalar mesons scales as predicted by the chromomagnetic interaction $[16, 17]$, $1/m_q m_Q$. This means a reduction around a factor 3 when going from open-charm to open-bottom mesons. In particular, while $M(\Delta \bar{D}^*) - M(\Delta \bar{D}) = 141$ MeV, $M(\Delta B^*) - M(\Delta B) = 45$ MeV what makes the coupled-channel effect much more important in the bottom sector and reverses the order of the two attractive channels, making the $(T, J) = (2, 3/2)$ state the lowest one. Similarly, the $(T, J) = (0, 1/2)$ channel, that is repulsive for the $N\bar{D}$ system, becomes attractive in the $NB$ case due to the coupled-channel effect, with a resonance at threshold. Thus, when going from the charm to the bottom sector in the baryon-meson open-flavor region, the number of states and their ordering may be modified due to the presence of nearby thresholds. Such effect seems hardly difficult to be predicted by any systematic expansion of the heavy quark sector.

Thus, as we had theoretically predicted in our benchmark calculation of Ref. [6], one observes how two effects come together to form a deeply bound state, the presence of two nearby thresholds and a strong coupling between them, in spite of the fact that the diagonal interactions of the different quantum numbers contributing to this state are not strong. Hence, threshold vicinity is a required but not sufficient condition to find a bound state. To illustrate our results, we have plotted in Fig. 3 the evolution of the binding energy of the $(T, J) = (2, 3/2)$ $N\bar{D}$ state if we artificially diminish the mass difference between the vector $\bar{D}^*$ and the pseudoscalar $\bar{D}$ mesons. We can see how a bound state arises when the thresholds come closer, around 120 MeV, without modifying the interactions entering the problem. Besides, the binding energy increases when the mass difference is reduced. This result poses an important warning when trying to extrapolate results of binding energies of
two-hadron systems to different flavor sectors. If the binding is mainly due to the vicinity of coupled thresholds, the increase on the mass of the two-hadron system may diminish the binding if it separates the thresholds \[9\]. Thus, if this mechanism is working for some of the recently discovered pentaquark states at the LHCb or the exotic states discovered in the hidden-charm or hidden-beauty meson spectra, the pattern expected on different flavor sectors may differ significantly as opposite to the charmonium and bottomonium spectra or the charm and bottom baryon spectra below open-flavor thresholds.

Let us finally note that the one-pion exchange plays a significant role in the $\Delta \bar{D} - \Delta \bar{D}^*$ and $\Delta B - \Delta B^*$ transition potentials, being the only contribution if quark-exchange effects were neglected (see Ref. \[11\] for details). As explained above, the mixing induced by the one-pion exchange, as well as quark-exchange contributions coming from the other terms of the interacting potential, comes enhanced due to the reduction of the mass difference between the two thresholds in the bottom sector. It has been recently argued in Ref. \[18\] the existence of an approximate light quark spin symmetry in $Z_b$ resonances, implying that the part of the interaction between heavy mesons that depends on the total spin of the light quark and antiquark is strongly suppressed. Unfortunately, this hypothesis cannot be tested in the system under study due to the presence of a single heavy antiquark. This symmetry will be proved in future works of $Z_c$ \[19, 20\] and $Z_b$ resonances \[21\] as well as the pentaquark
states reported at LHCb [1], where the mechanism proposed in this letter will be tested.

It is interesting to note that a similar argument has been drawn in Ref. [22] where the supercharmonium states, experimental resonances that appear to contain a $c\bar{c}$ pair, have been introduced but have other properties that preclude a description in terms of only $c\bar{c}$ (idealized charmonium) basis states. Four-quark supercharmonium configurations occur very near, or even below, the lowest S-wave threshold for production of meson pairs. These states evade Coleman’s argument in 1979 [23], who used the $1/N_c$ expansion of QCD to show that four-quark color singlets tend to propagate as pairs of mesons. One of these supercharmonium states could be the $Z(4475)$, that may appear as a linear superposition of $D\bar{D}^*$ mesons with one of them in a radially excited state $2S$. In a simple one-pion exchange model the $D \to D + \pi$ vertex is forbidden while the $D^* \to D + \pi$ is allowed. This gives rise to weak diagonal interactions but a strong mixing between two nearby thresholds, $D(1S)\bar{D}^*(2S)$ with a mass of 4482 MeV/$c^2$, and $D^*(1S)\bar{D}(2S)$ with a mass of 4433 MeV/$c^2$. The small mass difference between the thresholds due to the reduction of the hyperfine splitting when increasing the radial excitation leads to an amplification of the binding.

One can find also a similar situation in the heavy baryon spectra. An important source of attraction might be the coupled-channel effect of the two allowed thresholds, $(nnn)(Q\bar{n})$ and $(nnQ)(n\bar{n})$ [24]. When the $(nnn)(Q\bar{n})$ and $(nnQ)(n\bar{n})$ thresholds are sufficiently far away, the coupled-channel effect is small, and bound states are not found. However, when the thresholds get closer the coupled-channel strength is increased, and bound states may appear for a subset of quantum numbers. Under these conditions, there are states with high spin $J^P = 5/2^-$ that may lodge a compact five-quark state for all isospins [25]. The reason stems on the reverse of the ordering of the thresholds, being the lowest threshold $(nnn)(Q\bar{n})$ the one with the more attractive interaction. Of particular interest is the $(T)J^P = (2)5/2^-$ state, that survives the consideration of the break apart thresholds. It may correspond to the $\Theta_c(3250)$ pentaquark found by the QCD sum rule analysis of Ref. [26] when studying the unexplained structure with a mass of 3250 MeV/$c^2$ in the $\Sigma_{c}^{++}\pi^{-}\pi^{-}$ invariant mass reported recently by the BABAR Collaboration [27]. Such state could therefore be a consequence of the close-to-degeneracy of the lowest thresholds with $(T)J^P = (2)5/2^-$, $\Delta D^*$ and $\Sigma_c^*\rho$, and the attractive interaction of the $\Delta D^*$ system.

Summarizing, we have studied the $N\bar{D}$ and $NB$ two-hadron systems at low energies by means of a chiral constituent quark model. We have found a clear example of a baryon-
meson system, $NB$, where the vicinity of two different thresholds enhances the binding of a hadronic resonance as compared to the $ND$ system. As a consequence the pattern of states may change when moving among different flavor sectors, both in number and relative ordering of states, what poses a warning on extrapolations to heavy flavor sectors based on systematic expansions. When a resonance is controlled by a coupled-channel effect, going to a different flavor sector may enhance or diminish the binding. This effect may, for example, generate significant differences between the charmonium and bottomonium spectra above open flavor thresholds or pentaquark states in the open-charm and open-bottom sectors.

Acknowledgments

This work has been partially funded by Ministerio de Educación y Ciencia and EU FEDER under Contracts No. FPA2013-47443-C2-2-P and FPA2015-69714-REDT and by FAPESP grant 2015/50326-5.

[1] R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 115, 072001 (2015).
[2] T. J. Burns, Eur. Phys. J. A 51, 152 (2015).
[3] E. Braaten, Phys. Rev. Lett. 111, 162003 (2013).
[4] N. A. Törnqvist, Phys. Rev. Lett. 67, 556 (1991).
[5] Z. -F. Sun, J. He, X. Liu, Z. -G. Luo, and S. -L. Zhu, Phys. Rev. D 84, 054002 (2011).
[6] J. Vijande and A. Valcarce, Phys. Lett. B 736, 325 (2014).
[7] T. Fernández-Caramés, A. Valcarce, and J. Vijande, Phys. Rev. Lett. 103, 222001 (2009).
[8] T. Inoue, S. Aoki, T. Doi, T. Hatsuda, Y. Ikeda, N. Ishii, K. Murano, H. Nemura, and K. Sasaki, Nucl. Phys. A 881, 28 (2012).
[9] T. F. Caramés, A. Valcarce, and J. Vijande, Phys. Lett. B 709, 358 (2012).
[10] T. Hyodo, Y. -R. Liu, M. Oka, K. Sudoh, and S. Yasui, Phys. Lett. B 721, 56 (2013).
[11] T. F. Caramés and A. Valcarce, Phys. Rev. D 85, 094017 (2012).
[12] U. Wiedner (PANDA Collaboration), Future Prospects for Hadron Physics at PANDA, Prog. Part. Nucl. Phys. 66, 477 (2011).
[13] J. Vijande, F. Fernández, and A. Valcarce, J. Phys. G 31, 481 (2005).
[14] A. Valcarce, H. Garcilazo, F. Fernández, and P. González, Rept. Prog. Phys. 68, 965 (2005).
[15] H. Garcilazo, J. Phys. G 13, L63 (1987).
[16] N. Isgur, Phys. Rev. D 60, 054013 (1999).
[17] F. Close, AIP Conf. Proc. 717, 919 (2004).
[18] M. B. Voloshin, Phys. Rev. D 93, 074011 (2016).
[19] R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 112, 222002 (2014).
[20] K. Chilikin et al. (Belle Collaboration), Phys. Rev. D 90, 112009 (2014).
[21] A. Bondar et al. (Belle Collaboration), Phys. Rev. Lett. 108, 122001 (2012).
[22] T. Barnes, F. E. Close, and E. S. Swanson, Phys. Rev. D 91, 014004 (2015).
[23] S. Coleman, Aspects of Symmetry (Cambridge University Press, Cambridge, England, 1985), pp. 377-378.
[24] M. F. M. Lutz and E. E. Kolomeitsev, Nucl. Phys. A 755, 29c (2005).
[25] T. F. Caramés and A. Valcarce, Phys. Rev. D 90, 014042 (2014).
[26] R. M. Albuquerque, S. H. Lee, and M. Nielsen, Phys. Rev. D 88, 076001 (2013).
[27] J. P. Lees et al. (BABAR Collaboration), Phys. Rev. D 86, 091102(R) (2012).