Neural Network DPD for Aggrandizing SM-VCSEL-SSMF-Based Radio over Fiber Link Performance

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Abstract: This paper demonstrates an unprecedented novel neural network (NN)-based digital predistortion (DPD) solution to overcome the signal impairments and nonlinearities in Analog Optical fronthauls using radio over fiber (RoF) systems. DPD is realized with Volterra-based procedures that utilize indirect learning architecture (ILA) and direct learning architecture (DLA) that becomes quite complex. The proposed method using NNs evades issues associated with ILA and utilizes an NN to first model the RoF link and then trains an NN-based predistorter by backpropagating through the RoF NN model. Furthermore, the experimental evaluation is carried out for Long Term Evolution 20 MHz 256 quadrature amplitude modulation (QAM) modulation signal using an 850 nm Single Mode VCSEL and Standard Single Mode Fiber to establish a comparison between the NN-based RoF link and Volterra-based Memory Polynomial and Generalized Memory Polynomial using ILA. The efficacy of the DPD is examined by reporting the Adjacent Channel Power Ratio and Error Vector Magnitude. The experimental findings imply that NN-DPD convincingly learns the RoF nonlinearities which may not suit a Volterra-based model, and hence may offer a favorable trade-off in terms of computational overhead and DPD performance.

Keywords: digital predistortion; radio over fiber; neural network; error vector magnitude; adjacent channel power ratio

1. Introduction

The fifth generation, commonly known as 5G, of mobile networks is envisioned to uplift capacity, efficiency, capacity and latency [1]. Since 5G technology should address all application scenarios, third generation partnership project (3GPP) set the frequency limits in the 5G new radio (NR) standard, namely, frequency range 1 (FR1: 0.4–7.1 GHz range) and frequency range 2 (FR2: 24–52.6 GHz) [2].

Furthermore, due to an exponential increase in base stations (BS), the radio access network (RAN) has to be primarily centralized. A fronthaul (FH) is utilized for connecting baseband units (BBUs) and Remote Radio units (RRUs). The Centralized/Cloud Radio Access Network (C-RAN) primarily simplifies the network traffic and enhances the scalability (see Figure 1).

In this context, microwave photonics techniques such as radio over fiber (RoF) systems are the backbone of fed analog or digital signals in optical FH using RoF systems. RoF systems provide cost effective and beneficial solutions by escalating the extent of wireless links for short, medium and long reach networks [3,4]. Other than their significant highlights, such as immunity to electromagnetic interferences, low-loss and broad bandwidth, RoF links are liable to nonlinearities which can be solved using linearization methods [5–7]. RoF has many forms, such as analog radio over fiber (A-RoF) [1,3,4], digital radio over
fiber (D-RoF) [8,9] and Sigma Delta radio over fiber (S-DRoF) [10–12] systems. However, A-RoF suffers from nonlinearities, still due to the complexity of the other realizations and advantages in A-RoF that include simplicity, cost effectiveness and already widely spread legacy infrastructure, making it a better choice as compared to more efficient and costly solutions, such as D-RoF and S-DRoF [12].

 Analog fronthaul applications are limited due to the nonlinearities that arise due to microwave and optical parts. The amelioration of these nonlinearities has gained immense importance to increase the optical system capacity. Many nonlinearity mitigating techniques have been proposed in recent years to subdue these nonlinearities and improve the performance of such cost-effective systems [3,5–7,13–18]. However, these solutions have been questioned due to a limited bandwidth and need of feedbacking the output, which is an overlong process [5]. Similarly, for 5G networks, it would be strenuous to perform dynamic tracking while compensating the nonlinear channel response with broadband time varying data traffic from different RATs.

When we consider short range A-RoF links, the impact of impairments that arise due to concoction of fiber chromatic dispersion and laser frequency chirp is usually negligible [4,5]. However, still, the impact of signal impairments owing to the laser diode and photodiode is significant.

Similarly, these nonlinearities result in a rise of near channel interference and affect the quality of transmission. As explained in [6], similar to fifth generation (5G) and Long-Term Evolution (LTE) signals, Orthogonal Frequency Division Modulated (OFDM) signals are susceptible to distortions attributed to a high peak to average power ratio (PAPR) in their signal envelope [7]. These systems generate undesired spurious terms due to relatively stable causes such as nonlinear characteristic curves of lasers and possibly photodiodes. It is, therefore, necessary to reduce these spurious terms, to investigate optimal DPD techniques.

Moreover, in fiber-wireless integrated systems, the nonlinearities become serious when the analog fiber and wireless links are cascaded together [20]. They may arise due to the nonlinear laser transfer function [21,22], combined effect of laser chirp and fiber chromatic dispersion [23], fiber kerr nonlinearity [24] and various nonlinearities attributed to the microwave photonic link. The generation of inadmissible specious terms is due to nonlinear characteristics of lasers and perhaps photodiodes. Therefore, reducing these undesired terms can enhance performance.

Efficiently reducing these nonlinearities through linearization techniques has critical importance. In previous years, different linearization methods have been proposed [3,5–7,13–18].
however, digital predistortion (DPD) demonstrated itself as a successful technique in mollifying the impairments in RoF systems [15–18]. Traditional Volterra-based methods such as Memory Polynomial (MP) and Generalized Memory Polynomial (GMP) were used successfully in [15,17,18], reducing the laser nonlinearities. Similarly, a comparison was shown in [6] where DPD based on Canonical Piecewise Linearization (CPWL) outperformed the traditional Volterra methods by reducing the nonlinearities. Although the performance can be passable, the computation complexity needed for such methods can be extremely high requiring hundreds of coefficients and exhaustive training [18]. Similarly, these methods require the output to come to the central office during the periodical training phase. If the RoF uplink is set for this purpose, the nonlinearities in this case should be compensated. This feedback mechanism adds extra complexity to the process of DPD [6].

In recent years, machine learning (ML) solutions have advanced significantly. Neural networks (NNs) are expected to learn any nonlinear function; therefore, it becomes trivial that NNs can be used for predistortion. NN-based DPD will be very meaningful if we are able to circumvent the bottle neck that was created regarding the complexity of DPD due to Volterra-based methods.

NNs were applied for DPD in Power Amplifiers (PA) [25] that rely on indirect learning architecture (ILA) for training the predistorter. The ILA that was initially designed for NNs [26] was applied to DPD for the first time in [27]. As it is well known that in an ILA, a postdistorter learns an inverse model followed by its usage as a predistorter, the learning of a postdistorter is dependent on the noise in the feedback signal [25,28].

A detailed study on ML utilization for RoF systems was discussed in [29–32]. Zibar et al. in [29] discussed general optical communications and optical networks in terms of ML solutions. Whilst some works on the application of machine learning techniques in radio over fiber systems and networks have been reviewed, due to the general scope, the reviews in this field are relatively brief and limited. Recently, in [30,31], machine learning techniques were surveyed that include NNs, k-means technique, the convolutional neural network (CNN) and the reinforcement learning category. It also highlights different application scenarios. Recently, a Support Vector Machine (SVM)-based ML method was used to mitigate nonlinearities in A-RoF systems [31,32]. However, it is a non-NN-based solution.

Inspired by the NNs work on PA and the known problems of Volterra-based predistortion using ILA, we, for the first time, propose to counter the nonlinearities in A-RoF for Single Mode VCSEL (SM-VCSEL) using a Standard Single Mode Fiber (SSMF)-based RoF system with a novel DPD method that exploits NNs by evading the ILA.

Our proposed methodology is based on the fact that, firstly, we should look for an ideal RoF input signal as it is unknown. Since this ideal RoF input signal is unknown, an NN-based predistorter cannot be trained immediately in the first step.

After this step, an NN-DPD model is cascaded with the NN-RoF model. The ideal output of RoF is now known; therefore, it is a straightforward procedure to evaluate the error of the cascaded network (NN-DPD and RoF model). This error can then be backpropagated through the NNs, consequently updating the DPD-NN. This DPD NN can then be cascaded with the actual RoF link.

The NN-based predistorter is advantageous, as it is flexible as compared to Volterra-based methods. We have seen in [16–18] that the GMP model often requires many coefficients adding extra complexity and overheads. Contrarily, in NN-based DPD, this issue does not exist, as it should be able to learn all of the effects causing the error function; therefore, explicit designing of all possible causes of distortion in a model is not required. For instance, as explained in [33], if we want to correct for IQ imbalance, a simple Volterra-based method is unable to correct it. This requires an additional methodology to be implemented in the predistorter that further increases the complexity of the system manifolds. By the nature of the fully connected NN, the NN can learn such impairments and correct them.

The significant contributions of this paper are listed as follows:

1. A novel NN-based DPD algorithm is proposed for the linearization of RoF links.
2. This NN-DPD method has been implemented with a new training method without the utilization of indirect learning architecture where a separate RoF-NN is used to first model the RoF link. Once modelled, by back propagating the error through RoF-NN, the DPD-NN is trained.

3. The complexity of the proposed algorithms is estimated.

4. For the first time, an experimental comparative study has been conducted where DPD-NN, DPD-MP and DPD-GMP are compared in terms of Adjacent Channel Power Ration (ACPR) and Error Vector Magnitude (EVM).

The remaining part of the paper is organized as follows. Firstly, we discuss the architecture of the NN to perform DPD covering model overview, model characteristics, design and NN training. Then, a Volterra method-based methodology is discussed, and its architecture is explained. This is followed by complexity considerations of NN and GMP. Then, the section discusses the experimental setup utilized followed by a discussion of future directions. Finally, conclusions are presented.

2. Neural Network-Based DPD Architecture

The proposed NN DPD system is cascaded with the RoF link so that the overall result of this system will be a linear system. The proposed method is shown in Figure 2. It must be noted that training an NN requires training data, whereas the ideal NN output is not known. Since the ideal RoF output is known, an RoF NN model is trained to emulate the RoF link. By doing this, we can backpropagate through the RoF NN model to update the parameters in the NN DPD.

Consider that an RoF link with transfer function (discrete time domain) $H(n)$ will have output signal $y(n)$. Let us consider a complex baseband signal $x(n)$ that must be sent through an RoF link. The goal of DPD is to calculate the inverse transfer function of the RoF expressed as $I^{-1}$, which will then have an output of $\hat{x}(n)$. The simplified version can be expressed as:

$$\hat{x}(n) = \hat{I}^{-1}(x(n))$$  \hspace{1cm} (1)

while

$$y(n) = Gx(n) = I(\hat{x}(n))$$  \hspace{1cm} (2)
This means that NN is used to find \( \hat{I}^{-1} \) for predistortion. Since a training input and output sequence are required for NN training, however, the ideal \( \hat{I}(n) \) is not known and, therefore, a direct training to establish an NN for DPD is unachievable. We must note that ILA can be used for this identification; however, we would like to evaluate the other option for performance measurements (see Figure 3).

![Schematic showing RoF system utilizing a neural network (NN) digital predistortion (DPD) system and RoF NN model. After transmitting through the RoF link, the input and output of RoF are used to model RoF NN model \( \hat{I} \). Once trained, by backpropagating the error through \( \hat{I} \), training of \( I^{-1} \) is performed. This DPD RoF model is then used with the RoF link to perform linearization. Predistortion is carried out in a digital baseband so ADC and DACs are omitted.](image)

So, first of all, the second NN model is used to model the RoF link. Considering \( x(n) \) and \( v(n) \) as input and output data for the generic RoF link, training is carried out with the regression-based NN for these data, causing the NN to learn and identify the approximated transfer function \( \hat{I} \). Once the RoF NN model is established, the weights of the NN RoF model are fixed and it is connected to NN DPD. Consequently, the actual input \( x(n) \) and output training data are used to determine the error via loss function. This is then backpropagated via \( \hat{I} \) to train \( I^{-1} \).

### 2.1. NN Model Characteristics and Design

As far as structure of the NN is concerned, there are two NNs proposed and used in this project whose description is given below:

1. A DPD NN is utilized to predistort the “real” RoF link.
2. An RoF NN model is required to train the DPD NN.

The NN utilized in this work was a feedforward fully connected (FC) NN. The FC-NN contained \( N \) hidden layers and \( K \) neurons per hidden layer. The schematic of the structure utilized in NN is shown in Figure 4. Considering the complex baseband signal, the NNs have two inputs and two outputs, i.e., one for the real and the other for the imaginary part. For the hidden layer (one layer at least), ReLu was used. There are different sets of nonlinear activations that can be applied in the hidden layers; however, a rectified linear unit (ReLU) was chosen due to its lower complexity.

The output for the first hidden layer is expressed below in (3):

\[
I_1(n) = f \left( W_1 \left[ \frac{\Re(x)}{\|x\|} \right] + b_1 \right)
\]  

(3)

Here, \( I_1 \) represents the first hidden output layer, \( f \) represents the nonlinear activation function and \( W_1 \) and \( b_1 \) represent the weight and bias for the 1st output layer in NN.

Similarly, a general output for the \( i \)th layer can be expressed as:

\[
l_i(n) = f(W_i h_{i-1}(n) + b_i)
\]  

(4)
where \( i \in \mathbb{N} : 2 \leq i \leq N \) The final output after hidden layers \( N \) for the network is expressed in (5):

\[
\hat{x}(n) = W_{N+1}h_N + b_{N+1}
\]

(5)

Figure 4. Schematic showing block diagram of NN structure used in this article, feedforward fully connected (FC) NN. FC-NN contained \( N \) hidden layers and \( K \) neurons per hidden layer.

2.2. C. NN Training

The training algorithm for the NN DPD system is shown below (Algorithm 1). The mean square error is chosen as the loss function. ADAM is chosen as a standard optimizer. The update of weights is performed via backpropagation. In order to improve performance, the process can be repeated further for fine tuning of parameters for a total of \( Z \) iterations.

As explained earlier, the input and output data of “actual” RoF link are used to train NN that models the RoF link behavior. Once the model is obtained, a second DPD NN is connected to the RoF NN model. Once this training converges, the DPD NN is connected with the “real” RoF link to predistort it and conduct the parametric evaluation.

It is assumed that the training can be implied in an offline manner. Once the model is converged (learned), the model can run without any significant updates. However, occasional retraining may be required in some scenarios such as variation in temperature and length.

Algorithm 1. Training Performed

\[
\hat{x}(n) \leftarrow x(n)
\]

\[
\text{for } i \leq Z \text{ do}
\]

\[
y(n) \leftarrow I(\hat{x}(n)):\quad \text{// RoF Transmission}
\]

\[
\hat{I} \leftarrow \text{Train on } \hat{x}(n), \frac{y(n)}{G}:\quad \text{// Update RoF NN Model}
\]

\[
\hat{I} \leftarrow \text{Train on } x(n):\quad \text{// Freeze NN weights of } \hat{I}
\]

\[
\hat{x}(n) \leftarrow \hat{I}^{-1}(\hat{x}(n)):\quad \text{// Predistort}
\]

end for

3. Comparison with Volterra Method

It is interesting to observe the comparison of the NN DPD methodology with the conventional GMP method that was validated in [6,17]. MP and GMP are the most viable solutions that have been used for DPD. Since, in [6,15–17], it was established that GMP is better as compared to MP, for simplicity, evaluation with GMP is included in this paper.

3.1. Modelling Approach

The ILA is utilized for the DPD model coefficient computation, which is characterized in Figure 5. In the training phase, the coefficients for the predistortion are computed. As explained in [6], the input of predistorter \( z(n) \) comes through the RoF output \( y(n) \) where \( z(n) = y(n)/G \). \( G \) represents the gain of the RoF link. The estimation of coefficients is
performed using the least squares algorithm. As soon as the error \( e(n) \) converges, the coefficients are fed to the DPD block. The MP and GMP model utilized is discussed below.

The Memory Polynomial (MP) model is an inverse nonlinear model that has been previously used for direct and inverse modeling of power amplifier (PA) nonlinearities. The MP model is a conciliation between memoryless and full Volterra nonlinearity as it carries a diagonal memory. The output of the predistorter training block is in this case:

\[
z_p(n) = \sum_{k=0}^{K-1} \sum_{q=0}^{Q-1} c_{kq} z(n-q) |z(n-q)|^k
\]  

(6)

where \( c_{kq} \) is the model coefficients, \( K \) represents nonlinearity order, \( Q \) shows memory depth and \( z \) is the predistorter input sequence.

3.1.2. Generalized Memory Polynomial Model

The Generalized Memory Polynomial (GMP) method was implemented for VCSEL-based RoF in [15,17,18] and DFB-based links in [6,10]. The GMP model is evinced as:

\[
\hat{x}(n) = \sum_{k=0}^{K_a-1} \sum_{q=0}^{Q_a-1} c_{kq} x(n-q) |x(n-q)|^k + \sum_{k=1}^{K_b} \sum_{q=0}^{Q_b-1} \sum_{r=1}^{R_b} d_{kqr} x(n-q) |x(n-q-r)|^k + \sum_{k=1}^{K_c} \sum_{q=0}^{Q_c-1} \sum_{r=1}^{R_c} e_{kqr} x(n-q) |x(n-q+r)|^k
\]  

(7)

In Equation (7), \( x(n) \) and \( \hat{x}(n) \) represent the input and output, respectively, while \( c_{kq} \), \( d_{kqr} \) and \( e_{kqr} \) symbolize signal and envelope coefficients, signal and lagging envelope coefficients and signal leading envelope coefficients, respectively. \( K_a, K_b \) and \( K_c \) are the orders of nonlinearity; \( Q_a, Q_b \) and \( Q_c \) represent the depths of memory; \( R_c \) shows the leading and \( R_b \) symbolizes the lagging delay tap lengths, respectively.

3.2. Estimation Algorithm

The estimation starts with collecting the coefficients, e.g., \( c_{kqr}, d_{kqr} \) and \( e_{kqr} \), into a \( R \times 1 \) vector \( v \). \( R \) represents the total number of coefficients. \( v \) is associated with a signal whose time is sampled over the same period. Coefficients \( c_{21} \) are associated with signal \( x(n-1)|x(n-1)|^2 \). \( Z \) represents the collection of all such vectors into a \( N \times R \) matrix. Upon convergence, the output of the predistorter training block becomes \( z_p(n) = x(n) \), and hence, \( z(n) = u(n) \). For a total number of samples equal to \( N \), the output can be written as follows:

\[
z_p = Zv
\]  

(8)

Figure 4. Schematic showing block diagram of NN structure used in this article. Feedforward fully connected (FC) NN contained

Figure 5. Schematic of indirect learning architecture for the Memory Polynomial (MP)/ Generalized Memory Polynomial (GMP)-based DPD methodology.

3.1. Memory Polynomial Model

The GMP method was implemented for VCSEL-based RoF in [15,17,18] and DFB-based links in [6,10]. The GMP model is evinced as:

\[
\hat{x}(n) = \sum_{k=0}^{K_a-1} \sum_{q=0}^{Q_a-1} c_{kq} x(n-q) |x(n-q)|^k + \sum_{k=1}^{K_b} \sum_{q=0}^{Q_b-1} \sum_{r=1}^{R_b} d_{kqr} x(n-q) |x(n-q-r)|^k + \sum_{k=1}^{K_c} \sum_{q=0}^{Q_c-1} \sum_{r=1}^{R_c} e_{kqr} x(n-q) |x(n-q+r)|^k
\]  

(7)

In Equation (7), \( x(n) \) and \( \hat{x}(n) \) represent the input and output, respectively, while \( c_{kqr}, d_{kqr} \) and \( e_{kqr} \) symbolize signal and envelope coefficients, signal and lagging envelope coefficients and signal leading envelope coefficients, respectively. \( K_a, K_b \) and \( K_c \) are the orders of nonlinearity; \( Q_a, Q_b \) and \( Q_c \) represent the depths of memory; \( R_c \) shows the leading and \( R_b \) symbolizes the lagging delay tap lengths, respectively.
where \( z = [z(1), \ldots, z(N)]^T \) and \( z_p = [z_p(1), \ldots, z_p(N)]^T \), while \( \nu \) is a \( R \times 1 \) vector that contains the set of coefficients \( c_kq, d_{kqr} \) and \( e_{kqr} \). The LS solution is the solution for the following equation expressed as:

\[
\begin{bmatrix} Z^HZ \end{bmatrix} \hat{\nu} = Z^Hx
\]

The LS solution that minimizes the cost function is expressed as

\[
C = \sum_{n=1}^{N} |z_p(n) - x(n)|^2
\]

4. Complexity Considerations

The advanced variations in Volterra series can be obtained by changing memory depth and nonlinearity order to higher numbers. However, the computational complexity has to be considered as shown in Eq. 11. This means that while selecting the DPD model and its complexity, a smart tradeoff between complexity and performance can be made accordingly. For a comparative evaluation of NN and GMP methods in terms of complexity and performance, we evaluate expressions for each method in terms of its complexity. The total coefficients in the GMP method can be found by:

\[
K_a(Q_a + 1) + K_b(Q_b + 1)R_b + K_c(Q_c + 1)R_c
\]

Similarly, the numerals in the NN model are expressed as:

\[
(N - 1)K^2 + (4 + N)K + 6
\]

This means that in the case of NN, the complexity rises accordingly with the number of \( N \) hidden layers and \( K \) neurons per hidden layer. For instance, if we consider one layer, the complexity grows linearly by increasing neurons. However, if more than one layer is considered, with increasing the number of neurons, the complexity will scale quadratically. Similarly, if we consider GMP, there are eight parameters which can add to the complexity; however, for simplicity, if they are considered to be the same, the number of coefficients is 6 when all variables are kept equal to 1, and it increases to 546 if the variables are given the same value equal to 6.

The parameters utilized in the NN are summarized below in Table 1.

Table 1. NN specifications utilized.

| Specifications     | Values     |
|--------------------|------------|
| Optimizer          | ADAM       |
| Loss Function      | Mean Square Error |
| Hidden Layers      | 6          |
| Neurons per layer  | 25         |
| Hidden Layer Type  | ReLu       |
| Regularization     | L1         |

5. Experimental Setup

The experimental setup is presented in Figure 6, similar to the one that we presented in [17]; however, the DPD-NN-based method is an upgradation of this bench. An RoF link comprising an SM-VCSEL laser with an 850 nm wavelength is connected to a Standard Single Mode Fiber (SSMF) of 1 km. The optical signal is detected by a photodiode with a 3.4 GHz of bandwidth. The biasing current is set as 5 mA so that the power consumption is at an acceptable level, while the threshold current, is set to be 2 mA so that it is not very close to the threshold level. We use an inhouse software realized on MATLAB that emulates 20 MHz LTE with 256 QAM modulation baseband signal oversampled at 122.8 Ms/s. In
In the first phase, this signal is upconverted by a Vector Signal Generator (VSG) at a carrier frequency of 2.4 GHz. This is passed through an RoF link, and performance evaluation is carried out at the receiver with the Rohde and Schwarz FSW signal and spectrum analyzer used as a vector signal analyzer (VSA). In this step, the performance evaluation is recorded without the use of DPD block, i.e., No DPD.

In the second phase, the baseband signal oversampled at 122.8 MSa/s is fed into the DPD block and is upconverted at 2.4 GHz via VSG which is then fed to the optical link. The received signal at VSA is fed to the DPD training phase. Here, initially, the primary synchronization sequence and secondary synchronization sequence available in the LTE reference frames are engaged for synchronization between input and output (Figure 2). This block is responsible for the synchronization by finding the cross correlation by employing the M-part correlation method [34]. This operation is followed by employing the photodiode (PD) model to obtain the predistorter coefficients (Figure 2).

For the DPD validation phase, the switches move to the opposite direction, as shown in Figure 2. The evaluation is accomplished for the general LTE frames, which includes sampling, predistortion and passing them to the VSG. The nonlinear properties of the RoF link fluctuate slowly due to thermal effects and ageing of the components, which makes us assume that real-time processing in the adaptation is not required. Table 2 summarizes the parameters utilized in this work.

**Table 2.** Experimental setup parameter values.

| Link Components | Values |
|-----------------|--------|
| SM-VCSEL        |        |
| Wavelength      | 850 nm |
| $I_{bias}$      | 5 mA   |
| $I_{threshold}$ | 2 mA   |
| RIN             | $-130$ dB/Hz |
| SSMF            |        |
| Length          | 1 km   |
| Attenuation     | 3 dB/km |
| PD              |        |
| Responsivity    | 0.71 A/W |
| Bandwidth       | 2.5 GHz |
6. Experimental Results and Discussion

In this section, experimental results are presented and discussed. All the parameters utilized in these experiments are fixed. As mentioned before, 1 km SSMF is utilized, while memory depths $Q_a, Q_b, Q_c = Q = 2$ and nonlinearity orders $K_a, K_b, K_c = K = 1$ are also fixed. In addition to this, biasing and threshold currents for biasing SM-VCSEL laser are also fixed.

Figure 7 presents a comparison of experimental mean squared error (MSE) loss training for the NNs. It can be observed that the minimum MSE reached by the RoF NN model is 0.00189. This residue can be attributed to memory management and noise impairments in the data. Similarly, the DPD NN learns the predistortion profile for the RoF NN model. Once the learning converges, the DPD NN achieves an MSE approximately near to zero that equals $1 \times 10^{-5}$. It should be noted that this is a training loss for DPD with respect to the RoF NN model. On the basis of our previous findings in [6,12], we chose memory depths $Q_a, Q_b, Q_c = Q = 2$ and nonlinearity orders $K_a, K_b, K_c = K = 1$.

Figure 7. Experimental results for comparison of experimental MSE training loss for the NNs.

In Figure 8, the experimental findings are reported for ACPR for varying input powers. Since radio frequency (RF) input power can change with a change in application or scenario, it is of fundamental importance to check the effectiveness of the techniques used. The trend in Figure 8 confirms that the NN-based DPD method is performs better compared to GMP-based DPD. It can be noted that at a relatively higher RF input power of 5 dBm, the output ACPR is $-25$ dBc without DPD, $-35$ dBc with DPD-GMP and $-40$ dBc with the DPD-NN method, respectively.

Similarly, Figure 9 represents the Power Spectral Density (PSD), i.e., spectral regrowth of the received output signal with and without DPD for $P_{IN} = 0$ dBm. In the case of DPD, the two methodologies are shown. The DPD with GMP method is represented by the blue dashed line, while DPD-NN is shown using the green dash-dotted line. The output signal without DPD is shown by the red solid line. It can be observed that DPD-NN results in lower spectral regrowth with respect to GMP. Indeed, NN results in lower spectral regrowth as compared to GMP.
The trend in Figure 8 confirms that the NN-based DPD method is better compared to GMP. The dynamic range of NN results in better reduction as compared to GMP. The dynamic range of the NN method is 10 dBs higher than the GMP method. This further confirms that the NN method outperforms the GMP method by sweeping the RF input power. It is evident that EVM results also show that DPD NN results in better reduction as compared to GMP. The dynamic range of the NN method is 10 dBs higher than the GMP method. This further confirms that the NN method outperforms the GMP method.

In addition to ACPR evaluation, EVM performance is evaluated, depicted in Figure 10, by sweeping the RF input power. It is evident that EVM results also show that DPD NN results in better reduction as compared to GMP. The dynamic range of the NN method is 5 dBs higher than the GMP method. This further confirms that the NN method outperforms Volterra-based methods. The overall results are summarized in Table 3.

**Table 3.** Comparison among DPD methods for 0 dBm input power.

| Model | ACPR (dBc) | EVM (%) |
|-------|------------|---------|
| No DPD | −25 | 8 |
| MP | −35 | 2.2 |
| GMP | −40 | 2 |
| NN | −50 | 1.4 |

**Figure 8.** Experimental results for Adjacent Channel Power Ration (ACPR) results versus radio frequency input power for output with DPD-NN, DPD-MP, DPD-GMP and without DPD.

**Figure 9.** Spectral regrowth for output with DPD-NN, DPD-GMP and without DPD.
Conversely, the signal received by the RAU passes through (Ci) and is transmitted to the Optical UL up to the CO-BTS. Then, the signal is brought back to BB and processed by the sampled version of the baseband signal that was received at the RAU similarly to if the UL was/DNN) are fed to the PD Controller. The predistorter controller block is able to augment the memory of the model.

PAPR. Eventually, this will lead to an overall bandwidth elevation in the baseband waveforms would lead to elevated complexity of DPD performance due to vigorous computational handling of the task. From this experiment, we observe that training the model efficiency is converged in good proportions with one hidden layer and 30 neurons per memory of the model.

Confidence / Base Transmit Station (CO-BTS). In the figure, switches SW1, SW2 and SW3 are in configuration (1), and switches SW4 and SW5 are in configuration (2), while SW6, SW7 are not influential.

7. Real Time Realization of the NN DPD Method

Bringing the feedback signal from the BS to RAU is among the main challenging tasks in the adaptive recompense of the RoF link. This is due to possible nonlinearity of the feedback link; in fact, it can be as nonlinear as the RoF link, which is compensated for. The present work is based on the fact that the predistorter identifies only the nonidealities that it needs to compensate. Since it is assumed that the nonlinear feedback connection is uncompensated, it would destroy the performance of the compensation. In other words, this means that an approach is utilized where the RoF link is first compensated for using a postdistorter, and the known training signal from the RAU is used here. After that, the already compensated for downlink RoF link can be used as a feedback connection for the compensation [3].

However, as a possible feedback scenario, Figure 11 represents a realistic implementation of an adaptive DPD that shifts complex processing of the signals at the Central Office / Base Transmit Station (CO-BTS). In the figure, switches SW1, SW2 and SW3 are in configuration (1), and switches SW4 and SW5 are in configuration (2), while SW6, SW7 are not influential.

Figure 10. Experimental results for Error Vector Magnitude (EVM) received signal without and with linearization (DPD-NN and DPD-MP/GMP).

Figure 11. Possible realization of an adaptive predistortion scheme.

| Model       | EVM (%) |
|-------------|---------|
| No DPD      | 8.2     |
| With DPD MP | 6.8     |
| With DPD GMP| 5.2     |
| With DPD DNN| 4.8     |

Table 3. Experimental results for Error Vector Magnitude (EVM) received signal without and with linearization (DPD-NN and DPD-MP/GMP) for 0 dBm power signal, which is uncompensated, it would destroy the performance of the compensation. In other words, this means that an approach is utilized where the RoF link is first compensated for using a postdistorter, and the known training signal from the RAU is used here. After that, the already compensated for downlink RoF link can be used as a feedback connection for the compensation [3].

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However, as a possible feedback scenario, Figure 11 represents a realistic implementation of an adaptive DPD that shifts complex processing of the signals at the Central Office / Base Transmit Station (CO-BTS). In the figure, switches SW1, SW2 and SW3 are in configuration (1), and switches SW4 and SW5 are in configuration (2), while SW6, SW7 are not influential.

Figure 11. Possible realization of an adaptive predistortion scheme.

| Model       | EVM (%) |
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| No DPD      | 8.2     |
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| With DPD GMP| 5.2     |
| With DPD DNN| 4.8     |
This correlates to the “normal” operation of the bidirectional link. Indeed, the (DPD) is trained and performs a requisite processing of the digitized baseband signal, which is eventually brought back to analog form and modulated at radiofrequency (RF). After having passed through the Optical DL, the signal enters a circulator (Ci) that allows the transmission of the signal through a remote antenna unit (RAU).

Conversely, the signal received by the RAU passes through (Ci) and is transmitted to the Optical UL up to the CO/BS. Then, the signal is brought back to BB and processed by the CO-BTS (operation not shown). When switches SW4, SW6 and SW7 are set to configuration (3-A), and SW5 is connected to the ADC, a postdistortion operation is accomplished with reference to the UL. An RF test signal is sent through the Optical UL and arrives at the CO-BTS.

The characteristic parameters of the DPD methods (generalized/Memory Polynomials/DNN) are fed to the PD Controller. The predistorter controller block is able to augment the sampled version of the baseband signal that was received at the RAU similarly to if the operation of demodulation and sampling were performed at the RAU. It is anticipated that the nonlinear properties of the UL are stable across time, and so this process is seldom performed at the same frequency at which the DPD training is acquired.

The training of the digital predistorter is accomplished when switches SW1, SW2, SW3, SW4 and SW6 are set to configuration (3-B), while SW5 is connected to the ADC (SW7 not influent). This is the configuration described in the submitted work, where the digital predistortion block compares the transmitted and received sampled versions of the transmitted BB signal. It can be additionally discerned that a slight modification in the architecture shown in Figure 11 will utilize the Up-Link postdistortion mechanism for a reliable DPD feedback system.

8. Hardware Limitations

Machine learning solutions eminently depend on hardware resources for the computational handling of the task. From this experiment, we observe that training the model for 1 km of link length and utilized RF input power is not a tedious task. The training efficiency was converged in good proportions with one hidden layer and 30 neurons per layer. However, with optimized training, selection of the number of hidden layers and size of neurons per layer, linearization of longer link distances and higher bandwidths can be implied. Higher bandwidth signals such as multiple LTE carriers or 5G new radio (NR) waveforms would lead to elevated complexity of DPD performance due to vigorous PAPR. Eventually, this will lead to an overall bandwidth elevation in the baseband memory of the model.

9. Possible Future Directions

As far as future directions are concerned, the commercial viability of the current ML-based RoF networks is questionable. As pointed out in [30], hyperparameter selection is a critical point, as these parameters are tuned manually for now. There are no clear-cut rules or directions for the selection of these hyperparameters. Therefore, deep theoretical understanding of these ML algorithms is needed so they can be applied in practical RoF network management and resource allocation applications.

Similarly, availability of large data sets is a stringent prerequisite in terms of overhead, time and energy costs for using ML schemes effectively. This can be challenging for network failure-related training sets, as realistic networks have efficient designs that normally have the minimum possibility of network faults. As explained in [35,36], a possible solution is the transfer learning principle that eradicates the overheads linked with these trainings if the network changes relatively slowly over time.

Moreover, it is expected and also shown in this work that ML-based solutions will improve performance as compared to conventional methods, but this efficiency increase will involve additional costs, and this needs to be handled carefully.
10. Conclusions

This paper presents a novel unprecedented DPD-based NN architecture and training method for RoF link efficiency enhancement. A comparative evaluation study was carried out experimentally between NN- and Volterra (MP/GMP)-based DPD methods, and system potential was measured in terms of MSE, ACPR and EVM. The results validate that NN-based DPD reduces spectral regrowth by 22 dBs at 0 dBm of input power, and EVM is reduced from 8.1% to 1.5%, while the GMP-based method reduces ACPR by 14 dB and EVM to 2.3%. This asserts that an NN-based DPD method enhances the RoF link performance as compared to a GMP-based method already at a very low complexity. The extension of NN to include memory effects and tuning of hyper parameters for higher linearization link lengths and utilization of 5G NR multiband signals is envisaged in future work.

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