LSP baryogenesis and neutron-antineutron oscillations from R-parity violation

Lorenzo Calibbi, a Eung Jin Chun, b Chang Sub Shin c,d

a CAS Key Laboratory of Theoretical Physics, Institute of Theoretical Physics, Chinese Academy of Sciences, Beijing 100190, P. R. China
b Korea Institute for Advanced Study, Seoul 02455, Korea
c Asia Pacific Center for Theoretical Physics, Pohang 37673, Korea
d Department of Physics, Postech, Pohang 37673, Korea

E-mail: calibbi@itp.ac.cn, ejchun@kias.re.kr, changsub.shin@apctp.org

ABSTRACT: R-parity and baryon number violating operators can be allowed in the Supersymmetric Standard Model and thus lead to interesting baryon number violating processes such as n-\bar{n} oscillations and baryogenesis of the Universe via the decay of the lightest supersymmetric particle (LSP). Adopting the LSP baryogenesis mechanism realized by the late decay of the axino, we identify a single coupling \( \lambda''_{313} \) as a common origin for the matter-antimatter asymmetry of the Universe as well as potentially observable n-\bar{n} oscillation rates. From this, rather strong constraints on the supersymmetry breaking masses and the axion decay constant are obtained. The favoured parameter space of \( \lambda''_{313} \sim 0.1 \) and sub-TeV masses for the relevant sparticles is readily accessible by the current and future LHC searches.
1 Introduction

Unlike the Standard Model (SM), the Minimal Supersymmetric Standard Model (MSSM) may allow baryon and lepton number violating operators causing fast proton decay. Such a problem is often evaded by introducing a discrete symmetry, R-parity, enforcing baryon and/or lepton number conservation. When both baryon and lepton number violation are forbidden, the lightest supersymmetric particle (LSP) becomes stable and thus can be a good Dark Matter (DM) candidate if it is neutral. This has been considered as one of the good motivations for supersymmetry. On the other hand, the proton stability can be guaranteed by imposing only lepton number conservation. In this case, among the possible R-parity violating (RPV) terms, only baryon number violating (renormalizable) terms of the form

\[ W_B = \frac{1}{2} \lambda_{ijk}'' U_i^c D_j^c D_k^c \]  

are allowed in the MSSM superpotential. The above terms can lead to observable \( \Delta B = 2 \) processes like neutron-antineutron oscillations \([1–3]\) and di-nucleon decays like \( N N \rightarrow K K, \pi \pi \) \([4, 5]\) from a variety of diagrams involving supersymmetric particles and the \( \lambda_{ijk}'' \) interactions \([6–10]\). A new experiment has been proposed at the European Spallation Source (ESS) with the aim of improving the sensitivity to the neutron-antineutron transition probability by up to three orders of magnitude \([3]\).

The baryon number violation (BNV) allowed in the superpotential (1.1) could be a source of the matter-antimatter asymmetry of the universe \([11]\) through decays of the LSP that are induced by \( \lambda_{ijk}'' \) interactions. If baryogenesis occurred above the weak scale, a strong bound on \( \lambda_{ijk}'' \)

\[ \lambda_{ijk}'' \lesssim 10^{-6}, \]  

\[ (1.2) \]
can be set by requiring not to wash out the baryon asymmetry for squark masses around the TeV scale [12]. Such small couplings are not sizable enough to generate the observed baryon asymmetry. Thus one has to rely on baryogenesis at a very low temperature. Furthermore, the out-of-equilibrium decay of the LSP cannot lead to the desirable CP/baryon asymmetry at the usual second order of $\lambda''$ [13]. For these reasons, almost all the existing models implement the BNV baryogenesis mechanism by late decays of supersymmetric particles other than the LSP [14–19]. However, it was recognized in Ref. [20] that a LSP baryogenesis can be realized through the interference of a $\Delta B = 1$ (four quark) and $\Delta B = 2$ (six quark) operator at two loop. In this scenario, the LSP is considered to be the axino, a supersymmetric partner of the axion, as its interactions are suppressed by an intermediate axion scale $f_a \approx 10^{10–12}$ GeV leading to the late decay required for baryogenesis. Recall that the axion provides an elegant solution to the strong CP problem and, for values of the decay constant $f_a$ compatible with the above-mentioned range, it is a good Dark Matter candidate [21].

The purpose of this work is to investigate if the axino LSP baryogenesis can be implemented successfully by a certain BNV coupling which also leads to observable $n-\bar{n}$ oscillations. Following the idea of [20], we will consider the axino as the LSP decaying through a BNV coupling. In Section 2, we will identify the BNV coupling $\lambda''_{313}$ as a promising candidate, which can lead to an observable $n-\bar{n}$ oscillation consistent with our baryogenesis mechanism. The axino lifetime strongly depends on how to realize the axion mechanism. The two typical models by DFSZ [22, 23] and KSVZ [24, 25] will be considered in Section 3 and 4, respectively. A discussion of the parameter space compatible with baryogenesis and large $n-\bar{n}$ oscillation rates as well as of the impact of LHC searches for RPV supersymmetry will be given in Section 5. We conclude in Section 6.

2 Observable neutron-antineutron oscillations

In the presence of a $\Delta B = 1$ coupling in (1.1), the $\Delta B = 2$ operator like $(udd)^2$ or $(uds)^2$ arises after integrating out heavy squark fields to induce $n-\pi$ oscillations and/or di-nucleon decays. Currently the most stringent (direct) bound on $\lambda''_{ijk}$ comes from the $NN \rightarrow KK$ search [4]: $\lambda''_{112} < 10^{-6} - 10^{-7}$ for the squark masses in the TeV region [10], which is comparable to (1.2). Various couplings $\lambda''_{ijk}$ lead to the $n-\bar{n}$ oscillation operator

$$L_{n\bar{n}} = C_{n\bar{n}}(udd)^2 + h.c.$$

(2.1)

at tree or loop level in combination with flavor mixing among left-handed or right-handed squarks and possibly left-right squark mixing [6–9]. In fact, due to the contraction of the color indices in (1.1) through a totally antisymmetric tensor, the BNV couplings are antisymmetric under the exchange of the flavor indices of the $D^c$ superfields, $\lambda''_{ijk} = -\lambda''_{ikj}$, which implies that non-vanishing contributions to the $n-\bar{n}$ operator must involve squarks of the second or third generation mixing with the first generation. As a consequence, some of the strongest bounds can be put only in combination with squark flavor mixing such as $(\delta_{hR}^a)_{ij}$ (which parameterizes
the mixing among right-handed squarks): in [10], again assuming supersymmetric masses around the TeV, it was found $\lambda''_{11k}(\delta_{RR}^d)_{k1} \lesssim 10^{-8}$.

Barring additional degrees of freedom, we assume that no squark flavor mixing arises from supersymmetry breaking. Then, the flavor mixing can only arise from electroweak loop corrections – controlled by the Cabibbo-Kobayashi-Maskawa (CKM) matrix – that, however, hardly induce a sizable $n-\pi$ oscillation coefficient $C_{n\pi}$. One can find among various contributions that observable $n-\pi$ oscillations can be induced by $\lambda''_{113}$ or $\lambda''_{313}$ through electroweak one-loop diagrams [8, 9]. From the analysis of [10], one can see that the $\lambda''_{113}$ contribution to $C_{n\pi}$ is much larger than the $\lambda''_{313}$ contribution (involving a suppression from smaller CKM entries) for the same set of parameters, and thus observable $n-\pi$ rates from $\lambda''_{113}$ requires smaller values of the BNV coupling or a rather heavier supersymmetric spectrum. Such values make the axino decay much later than the Bing-Bang Nucleosynthesis (BBN) epoch and thus can not lead to a viable baryogenesis as will be shown in the following section. Therefore, the $\lambda''_{313}$ contribution remains to be a more favorable option for observable $n-\pi$ oscillations and baryogenesis.

We update the original contribution proposed by Chang and Keung (CK) [9] (whose diagram is depicted in Fig. 1) in a complete form properly taking the squark left-right mixing into account. Including only the lightest squark (stop or sbottom) contribution we find

$$C_{n\pi}^{CK} = \frac{g^4}{64\pi^2} (\lambda''_{313})^2 (V_{td}V_{ub})^2 m_{\tilde{\chi}^\pm} m_t m_b c_{\gamma_1} c_{\gamma_2} s_{\gamma_1} s_{\gamma_2}$$

$$J_6(m_{\tilde{t}_1}^2, m_{\tilde{b}_1}^2, m_{\tilde{\chi}^\pm}^2, m_W^2, m_T^2, m_B^2)$$

where $J_6(a_1, a_2, a_3, a_4, a_5, a_6) = \sum_{i=1}^{6} a_i \log a_i \prod_{k \neq i} (a_k - a_i)$. 

Figure 1. Electroweak loop diagram inducing $n-\pi$ oscillation from the $\lambda''_{313}$ coupling.
Here the effect of the left-right squark mixing is properly encoded in the squark mixing angle $\theta_{\tilde{q}}$ through the combination of $c_{\tilde{q}}s_{\tilde{q}} \equiv \cos \theta_{\tilde{q}} \sin \theta_{\tilde{q}}$. Taking for simplicity $m_{\tilde{q}} = m_{\tilde{t}} = m_{\tilde{b}} = m_S$ and maximal stop and sbottom mixing ($2c_{\tilde{q}}s_{\tilde{q}} = 1$ and $2c_{\tilde{b}}s_{\tilde{b}} = 1$), one finds the $n-\bar{n}$ oscillation time $\tau_{n\bar{n}} = 1/(C_{n\bar{n}} \langle n|(|udd|^2|\bar{n}) \rangle)$ as follows:

$$\tau_{n\bar{n}} \approx 10^9 \text{ sec} \left( \frac{2}{\lambda^{113}} \right)^2 \left( \frac{m_S}{500 \text{ GeV}} \right)^5 \left( \frac{0.5}{c_{\tilde{q}}s_{\tilde{q}}} \right) \left( \frac{0.5}{c_{\tilde{b}}s_{\tilde{b}}} \right) (250 \text{ MeV})^6 \langle n|(|udd|^2|\bar{n}) \rangle,$$

where we neglected and order-one prefactor variation in the loop function $J_6$ for different values of $m_S$. Taking into account the large uncertainty (of one order of magnitude or more) in the hadronic matrix element $\langle n|(|udd|^2|\bar{n}) \rangle$, the resulting oscillation time can be within the future sensitivitiy limit $\tau_{n\bar{n}} \approx 3 \times 10^9 \text{ sec}$ of the proposed experiment at the ESS [3], if indeed a $O(10^3)$ improvement on the limit set by [1] on the oscillation probability ($P_{n\bar{n}} \propto 1/\tau_{n\bar{n}}^2$) is achieved. In terms of the limit on the oscillation time, the bound of [1] reads $\tau_{n\bar{n}} > 0.86 \times 10^8 \text{ sec}$. While this was obtained directly employing free neutrons, the indirect limit from bounded neutrons in Super-Kamiokande is $\tau_{n\bar{n}} > 2.7 \times 10^8 \text{ sec}$ [2].

3 DFSZ axino baryogenesis

Let us first consider the DFSZ axion model to realize the axino LSP baryogenesis mechanism [20]. The axino ($\tilde{a}$) is the fermion component of the axion superfield,

$$A = (s + ia)/\sqrt{2} + \sqrt{2} \theta \tilde{a} + \theta^2 F_A,$$

where $a$ is the axion, $s$ is the saxion field. The $U(1)_{\text{PQ}}$ shift symmetry of the axion, under which $A \to A + i \alpha f_a$, is anomalously broken by the $SU(3)_C$ gauge symmetry. In the DFSZ axion model, the MSSM fields are also charged under $U(1)_{\text{PQ}}$. So the relevant interactions between $A$ and the MSSM fields are given by the $\mu$-term superpotential:

$$W = \mu e^{A/f_a} H_u H_d = \mu H_u H_d + \frac{\mu}{f_a} AH_u H_d + \cdots$$

From here we get the axino-Higgsino-Higgs interactions. Since the axino is the LSP in our scenario, the mixing between the axino and the Higgsino via the Higgs vacuum expectation value is important. For the axino-quark-squark interactions induced by the axino-Higgsino mixing, the axino decay rate follows from diagrams as those in Fig. 2. The corresponding operator can be obtained after integrating out the heavy squarks:

$$\mathcal{L}_{\text{decay}} = \frac{\lambda''_{ijk}}{f_a} \left( \frac{m_{\tilde{u}_i}}{m_{\tilde{u}_i}} \bar{u}_{\tilde{i}} d_j d_k + \frac{e^{-i\varphi_{\tilde{u}_i} m_{\tilde{u}_i}}}{m_{\tilde{u}_i}} \bar{u}_{\tilde{i}} d_j d_k + \text{h.c.} \right) + (u_i, \bar{u}_i \leftrightarrow d_j, \tilde{d}_j) + (u_i, \bar{u}_i \leftrightarrow d_k, \tilde{d}_k),$$

where $\varphi_{\tilde{u}_i} \equiv \text{Arg}(X_{\tilde{u}_i})$, with $X_{\tilde{u}_i} = A_{\tilde{u}_i} - \mu^* \cot \beta$ being the parameter that controls the squark left-right mixing, and

$$\frac{1}{m_{\tilde{u}_i}^2} \equiv \frac{\cos^2 \theta_{\tilde{u}_i}}{m_{\tilde{u}_i}^2} + \frac{\sin^2 \theta_{\tilde{u}_i}}{m_{\tilde{u}_i}^2}, \quad \frac{1}{m_{\tilde{u}_i}^2} \equiv \frac{\cos \theta_{\tilde{u}_i} \sin \theta_{\tilde{u}_i}}{m_{\tilde{u}_i}^2} - \frac{\cos \theta_{\tilde{u}_i} \sin \theta_{\tilde{u}_i}}{m_{\tilde{u}_i}^2}.$$
for the up-type left-right squark mixing angle $\theta_{\tilde{u}_i}$, and the corresponding squark mass eigenvalues, $m_{\tilde{u}_{i1}}$ and $m_{\tilde{u}_{i2}}(> m_{\tilde{u}_{i1}})$. Considering the coupling $\lambda''_{313}$, the axino decay is dominated by the top-quark channel mediated by $m_{\tilde{t}_1}$:

$$L_{\text{decay}} \simeq \frac{\lambda''_{313} m_t}{f_a m_{\tilde{t}_1}^2} \left( c_{\tilde{t}C} \overline{\tilde{a}} t d' b' + c_{\tilde{t}S} \overline{\tilde{a}} t e' d' b' + h.c. \right)$$  \hspace{1cm} (3.5)$$

where we neglected the heavier stop contribution and defined $\varphi_{\tilde{t}} \equiv \text{Arg}(X_t)$. For a successful late baryogenesis, the decay temperature $T_D$ of the axino LSP should be much smaller than the supersymmetry breaking scale but larger than the BBN temperature, that is, $1 \text{ MeV} \lesssim T_D \ll m_{\text{SUSY}}$. The decay rate reads

$$\Gamma_{\tilde{a}} \simeq \frac{|\lambda''_{313}|^2 m_t^2 |m_{\tilde{a}}|^5}{256 \pi^3 m_{\tilde{t}_1}^4 f_a^2},$$  \hspace{1cm} (3.6)$$

and from this we get for the axino decay temperature $T_D \approx \sqrt{\Gamma_{\tilde{a}} m_P}$:

$$T_D \approx 800 \text{ MeV} \left( \frac{|\lambda''_{313}|}{0.2} \right) \left( \frac{500 \text{ GeV}}{m_{\tilde{t}_1}} \right)^2 \left( \frac{|m_{\tilde{a}}|}{400 \text{ GeV}} \right)^{5/2} \left( \frac{10^{10} \text{ GeV}}{f_a} \right),$$  \hspace{1cm} (3.7)$$

which can be easily consistent with the BBN bound of $T_D \gtrsim 1 \text{ MeV}$. Notice that the other couplings $\lambda''_{ijk}$ with $i \neq 3$ can hardly satisfy the BBN bound due to the quark mass suppression of the axino coupling $\propto m_q / f_a$. For $\lambda''_{313} = \mathcal{O}(0.1)$, the NLSP will always prefer to decay into the SM particles, much faster than the BBN time. Therefore it is quite safe from the cosmological constraints. Instead it could give the interesting collider phenomenology which will be discussed in Section 5.

A CP asymmetry in the axino decay, as customary defined as

$$\epsilon \equiv \frac{\Gamma(\tilde{a} \to X) - \Gamma(\overline{\tilde{a}} \to \overline{X})}{\Gamma(\tilde{a} \to X) + \Gamma(\overline{\tilde{a}} \to \overline{X})},$$  \hspace{1cm} (3.8)$$

is generated by the interference between the tree-level diagrams in Fig. 2 and the two-loop diagrams obtained by joining the $\Delta B = 1$ diagrams of Fig. 2 with the $\Delta B = 2$ ones shown in

Figure 2. Tree-level diagrams for the decays of DFSZ type axino, $\tilde{a}$
Fig. 3. The calculation of the asymmetry gets simplified by considering the 6-quarks $\Delta B = 2$ operators that the diagrams of Fig. 3 give rise to, once the supersymmetric particles are integrated out. In general, the $\Delta B = 2$ operator $(tdb)^2$ is dominantly generated through the stop-stop-gluino exchange:

$$L_{\Delta B=2} = \frac{g_s^2 (\lambda''_{313})^2}{3|\tilde{m}_3|^2 m_{\tilde{t}_1}^4} \left( c_t^2 e^{-i\varphi_3} (t^c d^c b^c)^2 + c_t^2 s_t^2 e^{-i(2\varphi_1 - \varphi_3)} (\bar{t}d^c b^c)^2 \right) + h.c.,$$

(3.9)

where $\varphi_3 = \text{Arg}(m_{\tilde{g}})$. There are also contributions from the stop-sbottom-gluino exchange for $m_{\tilde{b}_1} \simeq m_{\tilde{t}_1}$. When the gluino is relatively heavier than the Wino-like neutralino $\tilde{W}^0$ (i.e. if $m_{\tilde{g}} \gtrsim (g_3/g)^2 m_{\tilde{W}} \simeq 3m_{\tilde{W}}$), the contribution from the stop-stop-$\tilde{W}^0$ diagram is also important:

$$L_{\Delta B=2} = \frac{g^2 (\lambda''_{313})^2}{4|\tilde{m}_{\tilde{W}}|^2 m_{\tilde{t}_1}^4} \left( c_t^2 e^{-i(2\varphi_1 - \varphi_{\tilde{W}})} (\bar{t}d^c b^c)^2 \right) + h.c..$$

(3.10)

Finally, the contribution from the RPV trilinear soft mass, $A''_{313} = |A''_{313}| e^{i\varphi_{313}}$, reads

$$L_{\Delta B=2} = \frac{|A''_{313}(\lambda''_{313})^2|(\lambda''_{313})^2}{m_{\tilde{t}_1}^2 m_{\tilde{d}_1}^2 m_{\tilde{b}_1}^2} \left( c_t^2 c_d^2 c_b^2 e^{-i\varphi_{313}} (t^c d^c b^c)^2 \right).$$

(3.11)
From (3.5, 3.9, 3.10, 3.11), we find the CP asymmetry from the axino decay:

\[ \epsilon = \frac{c_s^2 c_w^2 g^2 (\lambda_{313})^2}{32 \pi^3 m_3 \beta m_1 i} \mid \text{Im} \left[ \frac{m_2^2}{m_1^2} e^{i(\varphi_\alpha + \varphi_\beta)} + \frac{c_s m_1}{2 m_2} e^{i(\varphi_\beta - \varphi_\ell)} \right] \]

\[ + \frac{3 c_s^2 c_w^2 g^2 (\lambda_{313})^2}{128 \pi^3 m_3 \beta m_1 i} \mid \text{Im} \left[ \frac{s_\alpha^2 m_\alpha^2}{m_1^2} e^{-i(\varphi_\beta + \varphi_\alpha)} + \frac{c_s m_1}{2 m_2} e^{-i(\varphi_\beta - \varphi_\ell)} + \frac{c_s^2}{4} e^{-i(2 \varphi_\ell - \varphi_\beta + \varphi_\alpha)} \right] \]

\[ + \frac{c_s^2 c_w^2 g^2 (\lambda_{313})^2}{32 \pi^3 m_3 \beta m_1 i} \mid \text{Im} \left[ \frac{c_s^2 m_1^2}{m_2^2} e^{i(\varphi_\beta + \varphi_\alpha)} + \frac{c_s m_1}{2 m_2} e^{i(\varphi_\beta - \varphi_\ell)} + \frac{c_s^2}{4} e^{-i(2 \varphi_\ell - \varphi_\beta + \varphi_\alpha)} \right] \]

where \( \varphi_\alpha \) is the phase of the axino mass, \( m_\alpha \). For the gluino contribution, we see some additional suppressions compared to \( W^0 \) and \( A''_{313} \) term contributions because the strong interaction does not distinguish \( q \) and \( q' \), that is, gluino-quark-squark interactions preserve the change conjugation symmetry while the weak interaction and RPV terms strongly violate it. In particular, unlike the others, the gluino contribution is always proportional to powers of \( m_t/m_\alpha \) and vanishes for maximal left-right stop mixing: this reflects what we have just mentioned, namely that an asymmetry arises only in presence of chirality breaking. When the gauginos \( (\tilde{\lambda} = \tilde{g}, \tilde{W}^0) \) are light so that \( m_\lambda \sim m_\alpha \), the gaugino mass in the numerator should be substituted by \( 1/m_\lambda \to m_\lambda^2/(m_\lambda^2 - m_\alpha^2) \), which can provide a resonant enhancement to the asymmetry. Such an approximation is valid as long as \( m_\lambda - m_\alpha \gg \Gamma_\lambda \), a condition which we assume hereafter.

The CP asymmetry displayed in Eq. (3.12) depends on a number of unknown phases, some of which need to be \( O(1) \) in order to trigger a successful baryogenesis, as we are going to see. On the other hand, for TeV-scale supersymmetric masses, large phases in the sfermion and gaugino sectors would be tightly constrained by the experimental bounds on electric dipole moments (e.g. of the neutron and the electron), unless certain relations among generally independent phases are assumed (for a review see [26]). For simplicity here we are going to assume that the only large phase is the axino mass one, \( \varphi_\alpha \), which is left unconstrained by low-energy observables.

Numerically, the expression in Eq. (3.12) gives \( \epsilon \lesssim O(10^{-7} - 10^{-6}) \) for a choice of the parameters in the ballpark of Eq. (2.3), which give potentially large \( n - \bar{n} \) oscillation rates. The interplay between baryogenesis and \( n - \bar{n} \) oscillation will be discussed in greater detail in Section 5 together with the impact of searches for supersymmetric partners at the LHC. Provided that the stop mixing is large but not maximal, the gluino and wino contributions, i.e. the first and second lines of Eq. (3.12), give comparable contributions, while the A-term contribution (third line) is subdominant for \( \lambda''_{313} = O(0.1) \), as it is comparatively suppressed by a factor \( (\lambda''_{313})^2 \).

In order to achieve the observed baryon asymmetry, \( Y_{\Delta B} \simeq 0.8 \times 10^{-10} \) [27], a value of the CP asymmetry around \( \epsilon = O(10^{-7}) \) requires for the initial axino abundance \( Y_\alpha = n_\alpha/s \approx 10^{-3} \), which could arise from the thermal production of the DFSZ axino, \( Y^{TP}_\alpha \) for the reheating temperature greater than the Higgsino mass, and \( f_\alpha \lesssim 10^{10} \) GeV [28]. The actual value of \( Y_\alpha \) can be depleted from the initial (thermal) abundance because the long-lived axino.
can dominate the energy density of the Universe. Depending on the decay temperature, the final yield value is

$$Y_{\tilde{a}} = \min \left[ Y_{\tilde{a}}^{TP}, \frac{3 T_D}{4 m_{\tilde{a}}} \right].$$

(3.13)

Therefore the following constraint on the decay temperature (3.7) is imposed by a successful baryogenesis:

$$T_D \gtrsim \left( \frac{m_{\tilde{a}}}{\text{TeV}} \right) \left( \frac{\epsilon}{10^{-7}} \right) \text{GeV}$$

(3.14)

which is stronger than that from BBN. As we can see, this bound is fulfilled for values of the parameters in Eq. (3.7), translating in particular on a limit on the axion scale, $f_a \lesssim 10^{10}$ GeV. For these values of $f_a$, the axion misalignment mechanism can give a sizable contribution (up to 100%) to the observed DM abundance, provided a rather large value of the pre-inflation misalignment angle [29].

4 KSVZ axino baryogenesis

In the KSVZ axion model, the MSSM particles are neutral under the $U(1)_{\text{PQ}}$ symmetry, so there is no tree-level axino-squark-quark coupling. The leading interaction between the axino and the MSSM fields are given by the anomalous couplings induced by

$$\mathcal{L} \supset \int d\theta \frac{c_\alpha}{16\pi^2 f_a} A \mathcal{W}^\alpha \mathcal{W}_\alpha,$$

(4.1)

where $\mathcal{W}^a$ is the field strength chiral superfield for $SU(3)_C$. The axino can decay to three quarks at one loop through this axino-gluino-gluon interaction as shown in Fig. 4. After integrating out the squarks, we get the following effective Lagrangian for the axino decay:

$$\mathcal{L}_{\text{decay}} = -\frac{g^2}{(16\pi^2)^2} \frac{\lambda_{ijk}^\nu}{f_a} \ln \frac{f_a}{m_{\tilde{g}}^2} \left( \frac{e^{-i\phi_{\tilde{g}}}}{m_{\tilde{g}}} \bar{u}_i \tilde{d}_j \bar{d}_k + \frac{e^{-i(\phi_{\tilde{u}_i} - \phi_{\tilde{g}})}}{m_{\tilde{u}_i}^2} \bar{u}_i \tilde{d}_j \bar{d}_k + \text{h.c.} \right)$$

$$+(u_i, \tilde{u}_i \leftrightarrow d_j, \tilde{d}_j) + (u_i, \tilde{u}_i \leftrightarrow d_k, \tilde{d}_k)$$

(4.2)
As in the DFSZ case, the dominant Lagrangian term for the axino decay is

\[ \mathcal{L}_{\text{decay}} \simeq \frac{g_2^4}{(16\pi^2)^2} \frac{\lambda'_{313} |m_\tilde{g}|}{f_a m_{t_1}^2} \ln \left( \frac{f_a}{m_\tilde{g}} \right)^2 \frac{\left( \sum c_i e^{-i \phi^i} \bar{a} e^{i \theta^i} b^c + c_i^* e^{-i \phi^i} \bar{a} e^{i \theta^i} b^c \right) + h.c.}{m_\tilde{g}}. \] (4.3)

The corresponding axino decay temperature is

\[ T_D \simeq 200 \text{ MeV} \left( \frac{|\lambda'_{313}|}{0.2} \right) \left( \frac{500 \text{ GeV}}{m_{\tilde{g}}} \right)^2 \left( \frac{|m_{\tilde{g}}|}{400 \text{ GeV}} \right)^{5/2} \left( \frac{10^9 \text{ GeV}}{f_a} \right) \left( \frac{10^9 \text{ GeV}}{2 \text{ TeV}} \right). \] (4.4)

Compared to the DFSZ case, we obviously need smaller \( f_a \) to get a sizable decay temperature. The axino decay will generate the baryon asymmetry by the same \( \mathcal{L}_{\Delta B=2} \) operators in Eqs. (3.9, 3.10). The asymmetry parameter is rather insensitive to the decay rate, and thus we get a similar result as in the DFSZ case:

\[ \epsilon = \left| \frac{c_i^2(c_i^2 - s_i^2)g_2^2(\lambda'_{313})^2 m_{\tilde{g}}}{128 \pi^2 m_{\tilde{g}} m_{t_1}^2 m_{\tilde{W}}^2} \right| \left( \frac{c_i^2 m_{t_1}^2}{2|m_{\tilde{g}}|} e^{i(\phi^i - \phi^i_0)} + \frac{1}{4} e^{-i(\phi^i_0 + \phi^i_0)} \right) \] (4.5)

Again, one has to take the replacement: \( 1/m_{\tilde{\chi}} \rightarrow m_{\tilde{\chi}}/(m_{\tilde{\chi}}^2 - m_{\tilde{\chi}}^2) \) for the gauginos \( \tilde{\chi} = (\tilde{g}, \tilde{W}^0) \) when their masses are close to the axino mass \( m_{\tilde{a}} \). Comparing the above expression with Eq. (3.12) for the DFSZ case, we see that the gluino contribution has a term which is not suppressed by \( m_{\tilde{t}}/m_{\tilde{g}} \), because in the KSVZ case the axino decay is mediated by the gluino-quark-squark interaction which does not flip the chirality, while in the DFSZ case the axino decay rate is mediated by the Higgsino-quark-squark interactions which flip the chirality. This can make the asymmetry somewhat larger but still of the same order of magnitude, \( \epsilon \lesssim \mathcal{O}(10^{-7} - 10^{-6}) \).

The KSVZ axino thermal production is more active at higher temperature as long as \( T < f_a \), so that the final yield is sensitive to the reheating temperature of the Universe. Numerically, \( Y_a^{TP} \propto T_{\text{reh}} \). For a sufficiently high \( T_{\text{reh}} \), a sizable amount of \( Y_a^{TP} \) can be easily obtained. For example, when \( f_a \sim 10^9 \text{ GeV}, T_{\text{reh}} \gtrsim 10^5 \text{ GeV} \) is enough to make \( Y_a^{TP} \sim 10^{-3} \) [30]. Furthermore, such a thermal abundance can be reached even up to \( f_a \sim 10^{11} \text{ GeV} \) if the heavy quark mass is considerably smaller than the axion scale [31]. Including the case of axino dominated Universe before it decays, the actual yield value is

\[ Y_a = \min \left[ Y_a^{TP}, \frac{3 T_D}{4 m_{\tilde{a}}} \right] \gtrsim 10^{-3} \left( \frac{\epsilon}{10^{-7}} \right)^{-1}. \] (4.6)

From the expression for \( T_D \), Eq. (4.4), we find that the above bound can be fulfilled for values of \( f_a \) comparatively lower than in the DFSZ case. This makes it more unlikely to account for the full observed DM abundance in the KSVZ case.
5 Discussion

In this section we give a more quantitative discussion of the interplay between LSP baryogenesis and $n - \bar{n}$ oscillations. As we have seen in the previous sections, the magnitudes of both the CP asymmetry in the axino decay and the $n - \bar{n}$ oscillation time, $\tau_{n\bar{n}}$, can reach the desired levels for $\mathcal{O}(0.1)$ values of the RPV coupling $\lambda''_{313}$. Additionally, a large $\tau_{n\bar{n}}$ requires supersymmetric partners with masses $\lesssim 1$ TeV. Such a light spectrum has been extensively sought by the LHC experiments, although usual searches for supersymmetry requiring large missing momentum are insensitive to our case where R-parity is violated. In fact, although the axino LSP is long-lived on detector scales, the heavier supersymmetric particles, if produced in $pp$ collisions at the LHC, would eventually decay to SM quarks through $\lambda''_{313}$ rather than into the axino whose couplings are suppressed by the large scale $f_a$. Hence, the LHC phenomenology is dictated by the nature of the next-to-LSP (NLSP): heavier particles undergo decay chains ending with the NLSP, which decays to SM quarks. In particular, among the particles involved in the processes we are interested in, a stop NLSP would simply decay through the $\lambda''_{313}$ coupling as $\tilde{t}_1 \to b \bar{d}$ (analogously for a sbottom NLSP $\tilde{b}_1 \to t \bar{d}$), while if the NLSP is a gaugino, such as the Wino, it would decay to three bodies via an off-shell squark, e.g. $\tilde{W}_0 \to t \tilde{t}_1 \to t b \bar{d}$. In the large coupling regime we are interested in, $\lambda''_{313} = \mathcal{O}(0.1)$, both the above decays have large enough rates to occur promptly at the $pp$ interaction point.

A recent search (based on the full data-set of the 2016 LHC run at $\sqrt{s} = 13$ TeV) for pair-produced resonances each decaying into two jets (including b-jets) [32] – thus sensitive to direct production of stop pairs with the above RPV decay mode $\tilde{t}_1 \to b \bar{d}$ – excludes stop masses in the range $100$ GeV $< m_{\tilde{t}_1} < 470$ GeV and $480$ GeV $< m_{\tilde{t}_1} < 610$ GeV (the gap being due to what appears to be a slight statistical fluctuation). Similarly, other recent searches based on events with large jet multiplicities [33, 34] can be interpreted in terms of production of gluinos decaying into a top and a RPV-decaying stop, resulting in a limit on the gluino mass up to $m_{\tilde{g}} \lesssim 1.6$ TeV. The search of [33] has been also interpreted to constrain the case of stop production with the stops decaying into lighter charginos and neutralinos, hence addressing in our case the possibility of a Wino NLSP with the above-mentioned three-body decay. This sets a limit on the stop mass up to 1.1 TeV, but no bound is placed for a stop-gaugino mass splitting smaller than $m_t$, and similarly the sensitivity is rapidly lost if the stop is lighter than about 600 GeV. Finally, large RPV couplings can induce resonant single squark production at sizable rates, e.g. in our case $db \to \tilde{t}_1^*$. Based on this, several LHC searches with 8 TeV and early 13 TeV data have been employed in [35] to obtain upper limits on the $\lambda''_{ijk}$ couplings as a function of the squark mass: in particular $\lambda''_{313} \lesssim 0.2$ for $m_{\tilde{t}_1} < 1$ TeV.

The impact of the these searches on our parameter space is depicted in Figs. 5 and 6. In Fig. 5, we plot contours of the CP asymmetry in the decay of the DFSZ (first row) and KSVZ axino (second row) as a function of the coupling and a common mass $m_{\tilde{t}_1} = m_{\tilde{b}_1} = m_{\tilde{W}_0}$, together with the prediction for the $n - \bar{n}$ oscillation time. As we can see from Eq. (2.3), this observable strongly depends on the matrix element $\langle n | (u \bar{d}d)^2 | \pi \rangle$ whose value at present
Figure 5. Exclusion on the $n - \bar{n}$ oscillation time $\tau_{n\bar{n}}$ from [2] (solid blue line) and contours for several values of $\tau_{n\bar{n}}$ (dashed blue line) and the CP asymmetry $\epsilon$ (orange lines) induced by the axino in the DFSZ (first row) and KSVZ case (second row), displayed in the plane of a common mass $m_{\text{SUSY}}$ and $\lambda''_{313}$. Stop and sbottom mixing are taken as $\theta_{\tilde{t}} = \pi/6$ and $\theta_{\tilde{b}} = \pi/4$, and $\varphi_{\tilde{a}} = 1$ is the only non-vanishing phase. The other relevant parameters are as indicated in the plots. The light-green area is excluded by the ATLAS four-jets search [32]. The purple area is excluded by resonant stop production [35].

can be only estimated to be of the order of $\Lambda_{\text{QCD}}^6$. In order to take into account this large uncertainty affecting any prediction for $n - \bar{n}$ oscillations, we chose to show two ‘extremal’ values, $\langle n|\langle udd\rangle^2|\bar{n}\rangle = (200 \text{ MeV})^6$ (left plots) and $(300 \text{ MeV})^6$ (right plots), for which $\tau_{n\bar{n}}$ approximately spans one order of magnitude. The mass of the axino LSP is taken $m_{\tilde{a}} = 0.8 \times m_{\text{SUSY}}$, and large stop and sbottom mixing (respectively $\theta_{\tilde{t}} = \pi/6$ and $\theta_{\tilde{b}} = \pi/4$) as well
as $\varphi_a = 1$ for the axino phase are assumed. The areas excluded by the four-jets search [32] and resonant stop production [35] are shown in light green and purple respectively, while multijets searches [33, 34] are evaded for the heavy gluino mass $m_{\tilde{g}} = 2$ TeV that we chose. Although these LHC constraints are largely affecting our parameter space, we can see that they still leave room to values of the CP asymmetry, $\epsilon \approx 10^{-7} - 10^{-6}$, able to induce a successful baryogenesis (as discussed in Sections 3 and 4), with, at the same time, $n - \bar{n}$ oscillation times at the level of $\tau_{n\bar{n}} \approx 10^9 - 10^{10}$ sec. Furthermore, the bound from the four-jets search (light-green region) can be relaxed and eventually evaded taking $m_{\tilde{W}} < m_{\tilde{t}_1}$, as the stop will then preferably decay to neutralino or chargino. As we mentioned above, searches as in [33] can be in turn sensitive to the RPV decays of the Wino, but only for rather heavy MSSM particles and $m_{\tilde{t}_1} - m_{\tilde{W}} > m_t$. This is better illustrated by Fig. 6, where we set $\lambda^{\prime\prime}_{313} = 0.15$ and we plot our observables in the plane $m_{\tilde{t}_1} - m_{\tilde{W}}$, for two different values of the axino mass $m_{\tilde{a}} = 0.5 \times m_{\tilde{W}}$ (left panel) and $m_{\tilde{a}} = 0.8 \times m_{\tilde{W}}$ (right panel). Again the exclusion from the four-jets search is shown in light green, while the area to which the multijets search [33] is sensitive is dark green. Additionally, in the gray-shaded area the axino is not the LSP and the yellow band represents the LEP bound on the mass of charginos.

To summarize the above discussion, our scenario, despite the LHC constraints, can still achieve a large CP asymmetry (thus triggering LSP baryogenesis) and large $n - \bar{n}$ oscillation rates at the same time, provided that

- the RPV coupling is $\mathcal{O}(0.1)$;

Figure 6. Contours for $\tau_{n\bar{n}}$ and $\epsilon$ in the DFSZ scenario in the $m_{\tilde{t}_1} (= m_{\tilde{t}_1}) - m_{\tilde{W}}$. The values of the parameters were taken as in Fig. 5 unless otherwise indicated. The light-green area is excluded by the ATLAS four-jets search [32], the dark-green region by the multijets search [33]. The yellow region is excluded by LEP, while in the gray-shaded area the axino is not the LSP.
• stop and sbottom left-right mixing is large;

• an $\mathcal{O}(1)$ phase is present without inducing further constraints from CP-violating observables (a good example being the axino mass phase);

• the masses of the relevant supersymmetric particles, in particular $\tilde{t}_1, \tilde{b}_1$ and $\tilde{W}$ are $< 1$ TeV, thus at the level of the current sensitivity of searches for RPV supersymmetry at the LHC.

6 Conclusions

We have presented a scenario that consistently accounts for some formidable shortcomings of the Standard Model: the baryon asymmetry of the Universe, the observed amount of Dark Matter, the strong CP problem, as well as the hierarchy problem. The baryon asymmetry can be successfully produced by the decay of the axino LSP to SM quarks through RPV interactions, while DM and the strong CP problem are accounted for by the axion. We have shown that this is the case for both the DFSZ and the KSVZ axion models, although axion DM prefers the DFSZ scenario. In fact, in the DFSZ case, the requirement that the axino decays do not spoil BBN, i.e. $T_D > T_{\text{BBN}}$, and the more stringent one of having a sizable baryon asymmetry, $T_D \gtrsim \mathcal{O}(0.1 - 1)$ GeV are remarkably fulfilled for values of the PQ scale $f_a$ compatible with the observed DM abundance through the vacuum realignment mechanism of the axion field, although only for rather large values of the misalignment angle.

In our scenario, the LSP baryogenesis mechanism can be realized for a supersymmetric spectrum at the TeV scale. As we have shown, the same BNV interactions required by baryogenesis can then induce $\Delta B = 2$ processes such as neutron-antineutron at rates potentially observable by next-generation experiments. At the same time, large production rates of colored superpartners, in particular stops and gluinos, are possible at the LHC. This opens up the exciting possibility of testing our scenario in a number of experiments at very different energies: $n - \overline{n}$, LHC, as well as axion search experiments.

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