The cross-sectional shape and height expansion of coronal loops: High-resolution Coronal Imager (Hi-C) analysis of AR 12712

THOMAS WILLIAMS,1,2 ROBERT W. WALSH,1 AND HUW MORGAN2

1Jeremiah Horrocks Institute, UCLan, Preston, PR1 2HE, UK
2Department of Physics, Aberystwyth University, Penglais, Aberystwyth, SY23 3BZ, UK

(Received 18 June 2021; Accepted 27 June 2021)
Submitted to ApJ

ABSTRACT

Coronal loop observations have existed for many decades yet the precise shape of these fundamental coronal structures is still widely debated since the discovery that they appear to undergo negligible expansion between their footpoints and apex. In this work a selection of eight EUV loops and their twenty-two sub-element strands are studied from the second successful flight of NASA’s High resolution Coronal Imager (Hi-C 2.1). Four of the loops correspond to open fan structures with the other four considered to be magnetically closed loops. Width analysis is performed on the loops and their sub-resolution strands using our method of fitting multiple Gaussian profiles to cross-sectional intensity slices. It is found that whilst the magnetically closed loops and their sub-element strands do not expand along their observable length, open fan structures may expand an additional 150% of their initial width. Following recent work, the Pearson correlation coefficient between peak intensity and loop/strand width are found to be predominantly positively correlated for the loops (≈ 88%) and their sub-element strands (≈ 80%). These results align with the hypothesis of Klimchuk & DeForest that loops and – for the first time – their sub-element strands have approximately circular cross-sectional profiles.

Keywords: Sun: corona - methods: observational

1. INTRODUCTION

It has long been shown that coronal loops may have uniform cross sectional widths along their observable length (Klimchuk et al. 1992; Klimchuk 2000; Watko & Klimchuk 2000) where the cross-sectional profile is roughly circular. This behaviour is contrary to what one would expect; that is, flux tubes and thus coronal loops are expected to expand with height to maintain the pressure balance between the internal and external loop plasma due to gravitational stratification and decreasing magnetic field strength. This perceived circular cross-section may be explained by locally twisted flux tubes (Klimchuk et al. 2000; López Fuentez & Klimchuk 2006) which have been demonstrated to undergo less expansion than untwisted structures (McClymont & Mikic 1994).

The findings of Malanushenko & Schrijver (2013) offer an explanation for the perceived lack of expansion in loop observations that one would expect – the loops may have non-circular cross sections such as an ellipse. As noted by Klimchuk & DeForest (2020), if the expansion occurs preferentially along the line of sight, i.e. radially, rather than in the image plane, then no contradiction occurs. Malanushenko & Schrijver (2013) propose that because the coronal plasma is optically thin, loops expanding along the line of sight will be brighter in the image plane, which causes a selection bias as the brightness will decrease less rapidly as a function of height due to the increasing line of sight depth towards the apex. Whilst it is possible that the cross-sectional aspect ratio may change along a loop’s length, it is also possible that the aspect ratio remains fixed and merely rotates around a central axis, such as a twisting ribbon/rubber band (McCarthy et al. 2021). However, if that were the case then a loop would experience localised brightening and dimming along its length. That is, if we consider the twisting of an oval cross section, then there is more (less) material along the line of sight when the semi-minor (major) cross-sectional axis is lined preferentially with the observer, which leads to brighter (dimmer) intensity in the 2D projection of observational data due to the increased (decreased) plasma along the line of sight.

To test this hypothesis, Klimchuk & DeForest (2020) analyse the relationship between peak intensity and cross-sectional width of twenty coronal loops within the 193 Å High Resolution Coronal Imager (Hi-C; Kobayashi et al. 2014) data-set whose lengths are < 60 Mm. They find that these two properties were either positively correlated or uncorrelated but not negatively correlated, suggesting the cross-
sections of the loops could be approximately circular. More recently, McCarthy et al. (2021) utilised observations from two vantage points with 171 Å data from both Solar Dynamics Observatory’s (SDO) Atmospheric Imaging Assembly (AIA; Lemen et al. 2012) and Solar Terrestrial Relation Observatory’s (STEREO) Extreme Ultraviolet Imager (EUVI; Howard et al. 2008). From their sample of 151 loops, they identified thirteen as being suitable for width analysis. Utilising diameter-diameter measurements and peak intensity vs. loop width graphs, McCarthy et al. (2021) deduce that four of the thirteen loops may be elliptical with the remaining nine loops being approximately circular in shape. However, the diameter-diameter measurements are unlikely to be reliable given the lower resolution of EUVI, especially when AIA has been shown to be incapable of resolving – or in some instances detecting – narrower loops (Williams et al. 2020a).

As is discussed in Klimchuk (2000), the lack of cross-sectional expansion in loop observations have important implications for coronal heating models. The first is that energy may be deposited in an axial symmetric manner at the same spatial scales as the diameter of monolithic coronal loops/strands (full-width at half-maximum (FWHM) \( \lesssim 200 \text{ km}; \) Williams et al. 2020a,b). Alternatively, the energy deposited within strands and loops occur at spatial scales much smaller than the diameters of these structures – perhaps on spatial scales as small as 15 km (Peter et al. 2013) – and is then transported orthogonal to the loop abscissa in an axisymmetric manner. One popular mechanism for the latter scenario is the nanoflare heating model (Parker 1983, 1988) whereby field lines become braided and undergo small-scale magnetic reconnection due to photospheric motion at the footpoints.

In light of recent Hi-C findings indicating that monolithic loops may have approximately circular cross sections that exhibit no expansion along their observable length (Klimchuk & DeForest 2020), this paper employs the methods used in previous studies (§ 2) to examine the spatial scales along the loop envelope (Williams et al. 2020a) and individual loop sub-element strands (Williams et al. 2020b) of eight distinct coronal structures. In § 3, the relationship between loop width and their peak intensities are explored to classify whether their cross sections may be approximately circular (Klimchuk & DeForest 2020) or oval such as a twisted ribbon (Malanushenko & Schrijver 2013; McCarthy et al. 2021). For the first time, this study also extends this analysis to the sub-element strands contained within coronal loops and a discussion of these results in the context of current literature and the authors’ concluding remarks are presented in § 4.

2. DATA PREPARATION AND ANALYSIS METHOD

On 29th May 2018 at 18:54 UT, Hi-C 2.1 was successfully relaunched from the White Sands Missile Range, NM, USA, capturing high-resolution data (2k×2k pixels; 4.4′×4.4′ field of view) of target active region AR 12712 in EUV emission of wavelength 172 Å (dominated by Fe x emission \( \approx 0.8 \text{ MK} \)) with a plate scale of 0.129″. During the flight Hi-C 2.1 captured 78 images with a 2s exposure time and a 4.4s cadence between 18:56 and 19:02 UT. Full details on the Hi-C 2.1 instrument can be found in Rachmeler et al. (2019).

2.1. Data-set Extraction and Background Subtraction

The basis of the sample data-set investigated here include a number of subsets from the ten higher-emission cross-section slices analysed by Williams et al. (2020a) plus nine additional slices from within the Hi-C 2.1 field of view (see Figure 1 where all data-set locations are indicated). In each case the resulting emission profile across the structures would indicate sub-structure strands that are not fully resolved.

Following the method outlined in (Williams et al. 2020a), the Hi-C 2.1 data-set under consideration is time-averaged over a period \( \approx 60 \) s that is free from spacecraft jitter. Each cross-section normal to each strand is taken to be 3-pixels deep and the background emission is then subtracted. As outlined in Figure 2 of Williams et al. (2020b), this background subtraction is performed by firstly finding all the local minima of a slice, and interpolating through these values using a cubic spline (Yi et al. 2015) to obtain a global trend (dashed blue line). The global trend is then subtracted from the intensity profile along the slice, leaving behind the background subtracted coronal strands (similar to Aschwanden & Schrijver 2011; Williams et al. 2020a). Due to the large number of counts detected by Hi-C 2.1 the Poisson error associated with these isolated coronal strands is minimal.

2.2. Gaussian Fitting and FWHM Measurements

The analysis method is based on the assumption that at rest, an isolated coronal strand element has an observed emission profile across its width and normal to the strand axis that is approximately Gaussian. It is important to note that as indicated by Pontin et al. (2017), instantaneously coronal strands may not necessarily have a clear Gaussian cross-section. On the other hand, (Klimchuk & DeForest 2020) have shown from Hi-C observations that coronal strands are likely to have Gaussian cross-sections. The data samples are time-averaged over \( \approx 60 \) s (the first 11 Hi-C 2.1 frames) to average

1 A consequence of the instability experienced during the Hi-C 2.1 flight is that ghosting of the mesh could not be avoided (Rachmeler et al. 2019). This leads to the diamond patterns across the entire Hi-C 2.1 field-of-view, which are exaggerated when the data is enhanced with MGN (Figure 1).
out variations over short timescales, which helps address this issue. Whilst no obvious signs of motion within the structures analysed are noticed in this 60 s window, the authors acknowledge that as indicated by Morton & McLaughlin (2013), small amplitude oscillations could be present which would lead to the measured widths being broader than the structural width due to the time integration performed.

The observed Hi-C 2.1 intensity profile of a cross-sectional slice is reproduced by simultaneously fitting Gaussian profiles, the number of which is determined by the Akaike Information Criterion (Akaike 1974, AIC) along with a corrective term (AICc) for small sample sizes. This is fully described in the Appendix of Williams et al. (2020b). Subsequently, the full width at half maximum (FWHM) of the Gaussian profile is measured to provide an estimate of the possible width of the sub-structures likely present within the Hi-C 2.1 data.

Thus, the method employed to fit Gaussian profiles to the observed Hi-C 2.1 intensity is as follows. Firstly, the following expression for a Gaussian function, \( Y_G \) is used:

\[
Y_G = A \exp \left( -\frac{(x - x_p)^2}{2W^2} \right),
\]

whereby \( x \) is position along the cross-section slice, \( A \) and \( x_p \) are the amplitude and location of the peak, and \( W \) is the Gaussian RMS width. This can be related to the FWHM by:

\[
\text{FWHM} = 2 \sqrt{2 \ln 2} W \approx 2.35W.
\]

An estimate is made on the number of structures, \( N \) that could be present within the intensity profile along with their approximate location, width, and amplitude. Summing the \( Y_G \) values for \( N \) number of Gaussian curves at each pixel yields the model fit:

\[
f(x) = \sum_{i=1}^{N} Y_{G(i)}(x).
\]

The closeness of the fit at each pixel, \( \chi^2(x) \) is then determined by measuring the deviation of the fit from the original intensity:

\[
\chi^2(x) = \left( \frac{f(x) - y(x)}{\sigma(x)} \right)^2,
\]

where \( y(x) \) and \( \sigma(x) \) are the observed Hi-C 2.1 intensity and Poisson error at each pixel. The overall closeness of fit is then taken as \( \sum \chi^2(x) \), which is then reduced to its smallest value by simultaneously adjusting the free parameters \( A, x_p, \) and \( W \) for the \( N \) Gaussian curves in \( f(x) \).
curve fitting method, \textit{MPFIT}\textsuperscript{2} (Markwardt 2009) which is based on the MINPACK-1 FORTRAN library (Moré 1978). The one-\(\sigma\) uncertainties returned from \textit{MPFIT} are only accurate if the shape of the likelihood surface is well approximated by a parabolic function. Whether fitting multiple Gaussian profiles to each slice satisfies this condition or not would require analysis beyond the scope of this study, however, the one-\(\sigma\) uncertainties do provide a lower-bound of the FWHM errors.

To determine the appropriate number of Gaussian profiles, \(N\), within a given slice, the AIC model selection is employed. This is done by firstly generating several candidate models, where the number of Gaussian curves differs in each model. The non-linear least-squares curve fitting method is then employed for each candidate model and finally the AICc is then computed. The model with the smallest AICc value is then selected as the preferred model for that Hi-C 2.1 slice. Once the number of Gaussian profiles contained within a Hi-C 2.1 slice is determined, the strand width(s) are taken as the Gaussian FWHM value(s).

Klimchuk & DeForest (2020) states that this type of analysis is sensitive to background subtraction, and as such we find the number of Gaussian profiles fitted to a Hi-C 2.1 slice can be influenced by unwanted features such as other loops crossing in-front/behind the loop(s) or underlying moss regions. Whilst concerted efforts are made to avoid these regions, this is not always possible, and these unwanted “overlaps” of coronal structures result in differing numbers of sub-element strands being fitted by the AICc method compared to slices either side of the “overlaps”. Consequently, as this study aims to measure the changes in structural width and emission measure not only along loop segments but also along sub-element strands that may reside within these structures, a consistent number of Gaussian profiles is required to be fitted for the analysed portion of the loop(s). It is reasonable to assume the number of sub-element strands along a loop segment would be consistent and thus the cross-sectional slices where the number of Gaussian profiles determined by the AICc model selection do not match the modal value are likely to be contaminated with other coronal features along the line of sight. With this in mind, the sub-element strands are only analysed for the cross-sectional slices where the number of Gaussian profiles matches the modal value of Gaussian’s for the whole loop segment in question. A consequence of this conservative approach to fitting sub-element strands is that it is not always possible to analyse the structures along the entire loop segment. However, measuring the width of the loop envelope has no such constraints, and the method employed in Williams et al. (2020a) is adopted with the improved background subtraction discussed in Williams et al. (2020b).

3. RESULTS & ANALYSIS

A total of eight loops are selected from the Hi-C 2.1 field-of-view (FOV, Figure 1) that are relatively free from emission of surrounding coronal structures. From the selection of Hi-C 2.1 loops chosen for this study, loops A, B, C, and E are from open fan regions\textsuperscript{3} whilst loops D, F, G, and H are magnetically closed structures. In the analysis that follows, the orientation of loops D, F, and G are north-to-south (i.e. position 0 is at the top of the close-up images of Figure 1) whereas the other loops are orientated south-to-north such that the segments of the structures are traced away from their nearest footpoint. The AICc determined modal number of sub-element strands within loops A, D, E, G, and H is three, whilst loops B and C contain four strands, and Loop F has only two.

As can be seen in the FOV image, selecting a segment of a coronal loop that is isolated from surrounding coronal structures and the ghosting of the CCD mesh cells is a non-trivial task due to the abundance of loop-like structures and the underlying moss in AR 12712. Focusing on the close-up images of loops A - H in Figure 1 reveals that even the best-case loop segments we have selected here are not completely isolated from other coronal features or the mesh cell ghosting. For example, it is not possible to examine a longer portion of loop A as the segment analysed (denoted by the dashed line) is enclosed on both ends by the ghosting of a mesh cell. Similarly, despite loop D having a high contrast compared to the surrounding corona in the Multi-scale Gaussian Normalisation-enhanced images (Morgan & Druckmüller 2014), there are several structures that intersect the loop and thus affect the background subtraction.

3.1. Width Analysis

In Figures 2 and 3 the top panels labelled B1 – B6 and H1 – H16 show the Hi-C 2.1 cross-sectional intensity (blue), the AICc determined best-fit (red), and the Gaussian profiles (grey) that generate the fit. The intensity of these panels are normalised with respect to the maximum peak intensity of the loop segment being considered. The same figures for the other six loops are shown in the Appendix (Figures 6 – 11). In all these plots for loops A – H it is possible to follow the individual strands from one cross-sectional slice to the next along the loop segments analysed. As with previous results using this method (Williams et al. 2020b), the AICc determined fits closely match the observed Hi-C 2.1 cross-sectional profiles in most instances, with some minor excep-

\textsuperscript{2} MPFIT is freely-available at: http://purl.com/net/mpfit

\textsuperscript{3} Visual inspection of the AIA and EUVI full disc images support the expectation that these loops are fan structures and not large, closed loops.
Figure 2. Panels B1–B6 show the normalised Hi-C 2.1 intensities (blue), the AICc determined fit (red), and the Gaussian profiles (grey) generated to produce the fit for loop B. Emission is normalised with respect to the maximum peak intensity of panels B1–B6. The Gaussian profiles are numbered in accordance with the bottom panel which shows the loop (black) and strand (cyan, magenta, green, and orange) widths as a function of distance along the segment of the loop analysed. The error bars for the loop FWHM are $\pm 1$ Hi-C 2.1 pixel whereas the strand FWHM error bars are $5\times$ the one-$\sigma$ uncertainty returned from the curve fitting method. Note that Loop Position 0–15 Mm corresponds to south-to-north orientation in Figure 1.
Figure 3. Panels H1 – H16 show the normalised Hi-C 2.1 intensities (blue), the AICc determined fit (red), and the Gaussian profiles (grey) generated to produce the fit for loop H. Emission is normalised with respect to the maximum peak intensity of panels H1 – H16. The Gaussian profiles are numbered in accordance with the bottom panel which shows the loop (black) and strand (cyan, magenta, and green) widths as a function of distance along the segment of the loop analysed. The error bars for the loop FWHM are ±1 Hi-C 2.1 pixel whereas the strand FWHM error bars are 5× the one-σ uncertainty returned from the curve fitting method. Note that Loop Position 0 – 13 Mm corresponds to south-to-north orientation in Figure 1.
tions such as slices A3 and F6. Here, it would be possible
to reduce the deviance between the generated fits and the Hi-
C 2.1 emission by adding further Gaussian profiles, however,
in doing so the curve fitting model would no longer be sup-
ported by the AICc model selection method and would in-
crease the likelihood of over-fitting the data along the length
of the loop segments analysed.

The bottom panels of Figures 2 and 3 show the variation
in loop (black) and strand (cyan, magenta, green, orange)
widths as a function of loop position. The error bars for
the loop width indicate a Hi-C 2.1 pixel width (93.525 km)
whereas the error bars of the strands are the one-σ errors
returned from MPFIT. From the eight loops considered, six of
them show no signs of significant expansion, whereas the two
loops that do (B and E) are open fan structures and may be
expected to expand. Curiously, A and C are also open fan
structures yet their widths remain largely constant along the
segments analysed. It could be the case that these structures
have undergone expansion closer to the footpoints as with
loops B and E, however, this cannot be verified in this data-
set with our current methods.

Figure 4 shows the separation between the peak intensity
of neighbouring sub-element strands as a function of loop po-
sition for the loops A–H. Increasing loop position for loops
A, B, C, D, and H (E, F, and G) correspond to south-to-north
(north-to-south) orientation in Figure 1. Focusing upon the
six loops that show no obvious expansion, their sub-element
strands also exhibit no expansion (Figures 3, 6, 7, 8, 10, 11)
or separation between adjacent strands (Figure 4). Of these
loops, only loops C and F show initial and final widths that
are above the observational error of two Hi-C 2.1 pixel widths
(187.05 km). For loop C, this level of expansion is insignif-
icant (80 km above 2 Hi-C 2.1 pixels), and the close prox-
imity of a loop to the east whose intensity increases when
tracing the structure in a south-to-north orientation (Figure
1) may effect the background subtraction performed on loop C,
which would account for the decreased width seen from loop
position 14 Mm onward in Figure 7. For loop F, the width is
predominantly the same along the loop segment until a sud-
den decrease is seen in the final three cross-sectional slices
(Figure 10). As can be seen in the cross-sectional slices and
from the visual reference in Figure 1, the loop intensity de-
creases relative to the surrounding loop bundle and thus the
magnitude of the loop intensity relative to the background
emission that is subtracted decreases, which may contribute
to the contraction in loop width indicated in Table 1.

To quantify the total expansion ($\Gamma_{\text{tot}}$) of each loop/strand,
the final and initial widths of the segment analysed are calcu-
lated as the ratio

$$\Gamma_{\text{tot}} = \frac{W_{\text{final}}}{W_{\text{initial}}}.$$ 

The expansion rate ($\Gamma_{\text{rate}}$) is then simply expressed as

$$\Gamma_{\text{rate}} = \frac{\Gamma_{\text{tot}}}{t},$$
where \( l \) is the length of the loop/strand segment.

Employing this on loops B and E, it can be seen that they expand a total of \( \approx 860 \text{ km} \) and \( \approx 980 \text{ km} \), giving expansion rates \( (\Gamma_{\text{rate}}) \) along their lengths of 4.2 % and 6.8 % per Mm, respectively (Table 1). For Loop B, the widths of strands 1 and 2 remain within two pixel widths and as such do not contribute to the expansion of Loop B, whilst strands 3 and 4 expand \( \approx 500 \text{ km} \) and \( \approx 320 \text{ km} \). Furthermore, Figure 4 reveals that whilst the separation between strands 1 and 2 remains roughly constant, strands 2 and 3, and strands 3 and 4 spread apart along the loop segment under consideration. If we consider the findings of McClymont & Mikic (1994) that a twisted structure exhibits less expansion than an untwisted structure, then it may be that strands 1 and 2 are twisted structures whilst strands 3 and 4 are subjected to less twist and thus expand with height.

For loop E, all three strands show expansion above two pixel widths (\( \approx 260 \text{ km} \), \( \approx 460 \text{ km} \), and \( \approx 220 \text{ km} \), respectively) and the separation between all the sub-element strands also increases along the loop segment analysed. Thus, the expansion observed in the open fan structures B and E are the result of sub-element strands both expanding and separating from each other simultaneously.

### 3.2. Intensity vs. Width

Following the work of Klimchuk & DeForest (2020), this section investigates the relationship between the peak intensity and width of the selected loops and, for the first time, extends this analysis to their sub-element strands. As is discussed in Klimchuk & DeForest (2020), a negative correlation between width and intensity may indicate that a loop has an elliptical cross-section whereas if there is no or positive correlation, the cross-section is likely to be roughly circular.

Figure 5 top (bottom) shows the peak intensity of the loops (strands) as a function of FWHM. From visual inspection it can be seen that the peak intensities of loops B, C, and E appear strongly correlated to the widths of the structures whilst the remaining loops have weaker correlations where it is not possible to accurately determine whether the structures are positively or negatively correlated. As for the peak intensity of all the strands, they appear to predominantly be positively correlated to their widths – albeit to varying degrees with the strands of loop B showcasing the strongest correlation.

To quantify whether the peak intensity of cross-sectional slices along a segment of a loop/strand is positively or negatively correlated to the FWHM, the Pearson correlation coefficient is determined, the results of which are presented in Table 1. The Pearson correlation coefficient, \( P \) is defined as

\[
P = \frac{\text{cov}(\text{FWHM}, I)}{\sigma_{\text{FWHM}} \sigma_I},
\]

where \( \text{cov}(W, I) \) is the covariance of FWHM and intensity, whilst the denominator is the product of their standard deviations. If a structure has a positive (negative) Pearson correlation then as the width increases the intensity increases (decreases). The coefficient magnitude varies between -1 and 1 with values of \( P \approx 0 \) corresponding to uncorrelated data, whilst values of -1 and 1 correspond to perfectly correlated data.

From Table 1, it is found that all the peak intensities of the four open fan loops are positively correlated to their width, with loops B, C, and E being strongly correlated whilst loop A displays weak-to-moderate positive correlation. The weaker correlation of loop A is likely due to the fact that the structure exhibits minimal variation in the peak intensity and its width along the segment analysed, and so deducing a relationship between the two is more difficult. As for the sub-element strands within the four open fan structures, a total of three strands are negatively correlated (loop A, strands
Table 1. Pearson coefficients and expansion factors for all the loops/strands analysed.

| Structure | Loop Type | Pearson Coefficient | Initial Width (km) | Final Width (km) | Total Expansion | Expansion Rate (Mm⁻¹) |
|-----------|-----------|---------------------|--------------------|-----------------|-----------------|----------------------|
| Loop A    | Open Fan  | 0.198               | 899.3              | 754.9           | -0.161          | -0.005               |
| Strand 1  |           | -0.247              | 437.3              | 495.4           | 0.133           | 0.005                |
| Strand 2  |           | 0.715               | 375.5              | 281.8           | -0.249          | -0.008               |
| Strand 3  |           | -0.587              | 327.9              | 321.4           | -0.020          | -0.001               |
| Loop B    | Open Fan  | 0.995               | 976.5              | 1835.0          | 0.879           | 0.042                |
| Strand 1  |           | -0.926              | 665.3              | 488.5           | -0.266          | -0.021               |
| Strand 2  |           | 0.764               | 505.7              | 661.0           | 0.307           | 0.021                |
| Strand 3  |           | 0.981               | 293.8              | 791.9           | 1.696           | 0.102                |
| Strand 4  |           | 0.949               | 301.9              | 622.8           | 1.063           | 0.084                |
| Loop C    | Open Fan  | 0.772               | 1581.4             | 1314.1          | -0.169          | -0.169               |
| Strand 1  |           | 0.931               | 791.2              | 673.9           | -0.148          | -0.011               |
| Strand 2  |           | 0.733               | 790.5              | 690.2           | -0.127          | -0.008               |
| Strand 3  |           | 0.911               | 470.6              | 404.6           | -0.140          | -0.009               |
| Strand 4  |           | 0.538               | 490.5              | 387.7           | -0.210          | -0.014               |
| Loop D    | Closed    | 0.314               | 784.7              | 768.6           | -0.021          | -0.001               |
| Strand 1  |           | 0.525               | 768.9              | 403.6           | -0.475          | -0.031               |
| Strand 2  |           | 0.105               | 447.2              | 568.4           | 0.271           | 0.018                |
| Strand 3  |           | 0.465               | 442.6              | 493.2           | 0.115           | 0.007                |
| Loop E    | Open Fan  | 0.869               | 651.9              | 1631.1          | 1.502           | 0.068                |
| Strand 1  |           | 0.844               | 510.5              | 768.3           | 0.505           | 0.027                |
| Strand 2  |           | 0.947               | 286.3              | 749.7           | 1.618           | 0.073                |
| Strand 3  |           | 0.789               | 297.1              | 513.6           | 0.729           | 0.038                |
| Loop F    | Closed    | 0.384               | 1664.0             | 1199.8          | -0.279          | -0.010               |
| Strand 1  |           | 0.016               | 1096.0             | 1091.1          | -0.004          | < -0.001             |
| Strand 2  |           | 0.464               | 745.3              | 801.5           | 0.075           | 0.003                |
| Loop G    | Closed    | 0.312               | 1054.4             | 1096.2          | 0.040           | 0.003                |
| Strand 1  |           | 0.143               | 694.8              | 651.1           | -0.063          | -0.004               |
| Strand 2  |           | 0.490               | 434.7              | 447.9           | 0.030           | 0.002                |
| Strand 3  |           | -0.053              | 429.4              | 359.7           | -0.162          | -0.010               |
| Loop H    | Closed    | -0.437              | 1208.5             | 1100.5          | 0.052           | 0.003                |
| Strand 1  |           | 0.388               | 947.7              | 693.3           | -0.268          | -0.014               |
| Strand 2  |           | 0.395               | 630.5              | 565.5           | -0.103          | -0.006               |
| Strand 3  |           | 0.520               | 674.6              | 413.6           | -0.387          | -0.207               |

1, 3 and loop B, strand 1), with the remaining eleven all exhibiting strong positive Pearson correlation coefficients. This indicates that as the structures broaden, peak intensities increase for open fan loops and their sub-element strands.

As for the magnetically closed structures, three of the four loops (D, F, and G) are positively correlated whilst loop H is negatively correlated. All four loops have modest Pearson correlation coefficient magnitudes that are weaker than all the open fan loops bar loop A. Peculiarly, all the Pearson coefficients bar one of the sub-element strands are positively correlated for the magnetically closed structures despite the fact that loop H is negatively correlated. The other strand (loop G, strand 3), whilst having a negative Pearson coefficient, the absolute magnitude is such that the strand exhibits no linear correlation and thus is considered to be uncorrelated.

Focusing on loop H, the loop width broadens as one travels along loop position (Figure 3 bottom) whilst the peak intensity of the cross-sectional slices decreases (Figure 3 H1 – H16). Thus, there should be a negative correlation between the intensity and width for the loop. If we now consider the sub-element strands, such as strand 2 say, it can be seen that as the peak intensity fluctuates, the FWHM remains relatively constant along the analysed segment whilst the spacing between strands 1 and 2 (2 and 3) increases (decreases) (Figure 4) as the loop expands, i.e. the strands spread out (overlap more) along the integrated line-of-sight. All these
factors together may explain a weak positive Pearson correlation coefficient for the strands of loop H despite the loop being negatively correlated.

As is noted in Klimchuk & DeForest (2020), if a loop or strand were to be non-circular (such as an oval) and twisted, there would be an inverse relationship between the intensity and width. That is, the loop would have a higher (lower) peak intensity at narrower (broader) loop widths if relatively constant density and temperature are assumed. The majority of our results for open fan and closed loops, along with McCarthy et al. (2020), and nine of the thirteen structures analysed by McCarthy et al. (2021) indicate that the relationship between intensity and width may be positively correlated and thus their cross sections are approximately circular. However, it is worth noting that one magnetically closed loop, and three open fan strands of this study along with four loops analysed by McCarthy et al. (2021) do support the idea that some loops and sub-element strands may be non-circular.

4. CONCLUDING REMARKS

Employing the analysis methods of Williams et al. (2020a,b), this article investigates the relationship between width and peak intensity of eight relatively isolated coronal loops and extends this for the first time to sub-element strands within the Hi-C 2.1 data. These loops and strands are traced along segments 10 – 30 Mm in length, which are of comparable length to the loops analysed with the data from the first Hi-C mission (Klimchuk & DeForest 2020) but are some 20 – 50 Mm shorter than those in the recent study by McCarthy et al. (2021).

The population of the eight loops analysed is evenly split between open fan (loops A, B, C, and E) and magnetically closed (loops D, F, G, and H) structures and are thus treated independently from each other in our width expansion analysis. The segments analysed for loops B and E reside near the visible footpoints (Figure 1) of the open fan structures and thus undergo significant expansion whereby their widths increase an additional 80% and 150% (see Total Expansion, Table 1) of their initial value. Conversely, the segments analysed for loops A and C (Figures 6 and 7) show minimal width variation along their length. These results suggest that open fan loops may expand rapidly near their footpoints and after which their cross-sectional width may remain relatively constant. With that said, a more comprehensive data-set is required from future high resolution missions to confirm this as current and archival data lack the resolving power to accurately quantify the expansion seen with Hi-C 2.1.

As with previous loop width studies (Klimchuk et al. 1992; Klimchuk 2000, 2015; López Fuentez & Klimchuk 2006), the magnetically closed structures analysed in this article exhibit little expansion with three of the four loops showing < 6% (108 km; < 1.2 Hi-C 2.1 pixels) expansion (Table 1) along the analysed segments. Similarly, the width and separation distance of the sub-element strands of these loops remain largely constant along the loop portions under consideration in this study. One caveat to this is that loop D can be seen to expand and contract periodically.

As discussed by Klimchuk & DeForest (2020), the largest error in coronal loop width analysis is a direct result of performing background subtraction due to the relative magnitudes of the loop and line-of-sight emission that is removed. Close inspection of the FOV image (Figure 1) reveals multiple structures intersecting/crossing loop D, which makes it more difficult to employ a consistent background removal along the loop segment. As such, these variations in loop width are likely to be the caused by background subtraction due to the crossing of multiple structures along the line-of-sight rather than because the loop is a twisted structure of non-circular cross-section (Malanushenko & Schrijver 2013).

Generalising the data-set as a whole, the expansion of loops can be quantified by the sub-element strands broadening and separating from each other simultaneously along the segments considered which leads to the increasing cross-sectional loop widths seen in loops B and E. Similarly, the lack of expansion seen in the other six structures is caused by strands whose widths and separation remain relatively constant along the loop segments analysed.

Upon exploring the relationship between loop width and peak intensity, this article finds that seven of the eight loops analysed (≈ 88%) are positively correlated, with the other loop being negatively correlated. These results match previous findings (West et al. 2014; Kucera et al. 2019; Klimchuk & DeForest 2020) with Klimchuk & DeForest (2020) being a notable comparison due to their work also examining loops of similar lengths to the ones in this study with Hi-C, albeit with the 193 Å data-set. As such, our results support the Klimchuk & DeForest (2020) hypothesis that loops are more likely to exhibit circular cross sections rather than elliptical ones (Malanushenko & Schrijver 2013; McCarthy et al. 2021), which would be the case if the peak intensities and widths of the cross sectional slices were negatively correlated. As for the coronal strands, we obtain a similar outcome with 20 strands (80%) showing positive correlation, 3 strands (12%) showing negative correlation and 2 strands (8%) being uncorrelated.

The findings presented in this article for magnetically closed coronal loops and their sub-element strands support the discussion of Klimchuk (2000) and Williams et al. (2020a,b) in regards to coronal heating. That is, whatever mechanism is responsible for the coronal heating, theoretical models may need to reproduce monolithic strands whose cross-sections (i) have widths at the same order of an AIA pixel (≈ 435 km), and (ii) are approximately circular along
their length. These implications for coronal heating are contingent on coronal loops being compact structures that are subjected to twist. In particular, fitting multiple nearly-cylindrical Gaussian-shaped strands relies heavily on the assumption that curvilinear features in the Hi-C 2.1 image plane do indeed correspond to compact structures in three dimensions. Whilst this assumption is plausible, other explanations may be equally valid in explaining the cross-sectional profiles observed. As is discussed in McCarthy et al. (2021), monolithic loops when viewed from a single vantage point – such as AIA or in this study Hi-C 2.1 – may in fact be loops with non-fixed aspect ratios and/or exhibit anisotropic expansion. They may also be the result of projection effects of complicated bright manifolds in the corona, or some other complex density enhancement. Thus, further three-dimensional analysis is required to confirm whether coronal loops are possibly well represented by a collection of sub-element strands.

As with the West et al. (2014) (11 loops), Klimchuk & DeForest (2020) (20 loops) and McCarthy et al. (2021) (13 loops) studies, this analysis is on a small sample size – largely due to the difficulty in tracing isolated segments of coronal loops within the Hi-C 2.1 data – and as suggested by Malanushenko & Schrijver (2013) may be subject to selection bias. Further high resolution data is required, such as from Solar Orbiter’s Extreme Ultraviolet Imager (EUI; \( \approx 0.1'' \) pixel\(^{-1} \) at 0.28 AU) instrument, to explore the relationship between intensity and width in the hope of understanding the fundamental geometry of these important structures in the quest for solving the coronal heating problem.

TW and HM gratefully acknowledge support by Leverhulme grant RPG-2019-361. HM also acknowledges STFC grant ST/S000518/1.

APPENDIX

A. FITTING CORONAL LOOP SUB-ELEMENTS

In this appendix, the additional figures discussed in § 3 are presented. In Figure 6, the top panels (A1 – A20) show the normalised Hi-C 2.1 intensity slice (blue) and the Gaussian profiles (grey) that are used to generate the fit (red). The cross-sectional profiles are each normalised to the maximum intensity of the loop segment. The bottom panel shows the cross-sectional width of the loop (black) and the sub-element strands (cyan, magenta, green) as a function of position along the loop segment. The error bars for the loop widths indicate \( \pm 1 \) Hi-C 2.1 pixel whilst the error bars of the sub-element strand widths are the one-\( \sigma \) errors returned from the curve-fitting method. The same plots are shown for loops C (Figure 7), D (Figure 8), E (Figure 9), F (Figure 10), and G (Figure 11). As can be seen from these figures, magnetically closed loops, D, F, and G, and open fan loops A and C show little variance in the cross-sectional loop width vs. length, whilst open fan loop E undergoes significant expansion.

REFERENCES

Akaike, H. 1974, ITAC, 19, 716
Aschwanden, M. J., Peter, H. 2017 ApJ, 840, 4
Aschwanden, M. J., Schrijver, C. J. 2011, ApJ, 736, 102
Bray, R. J., Cram, L. E., Durrant, C., Loughhead, R. E. 1991, Plasma Loops in the Solar Corona (Cambridge: Cambridge University Press)
Brooks, D. H., Warren, H. P., Ugarte-Urra, I., Winebarger, A. R. 2013, ApJL, 772, L19
Brooks, D. H., Reep, J. W., Warren, H. P. 2016, ApJL, 826, L18
Burnham, K. P., Anderson, D. R. 2002, Model Selection and Multimodel Inference: A Practical Information-Theoretic Approach (New York: Springer-Verlag)
Cirtain, J. W., Del Zanna, G., DeLuca, E. E., Mason, H. E., Martens, P. C. H., Schmelz, I. T., ApJ, 655, 598
Cirtain, J. W., Golub, L., Winebarger, A. R., et al. 2013, Nature, 493, 501
De Pontieu, B., Title, A. M., Lemen, J. R., et al. 2014, SoPh, 289, 2733
Fredvik, T., Kjeldseth-Moe, O., Haugan, S. V. H., et al. 2002, Adv.Space Res., 30, 635
Howard, R. A., Moses, J. A., Vourlidas, J. S., et al. Space Sci. Rev., 136, 67
Kobayashi, K., Cirtain, J., Winebarger, A. R., et al. 2014, SoPh, 289, 4393
Klimchuk, J. A., Lemen, J. R., Feldmen, U., Tsuneta, S., Uchida, Y. 1992, PASJ, 44, L181
Klimchuk, J. A. 2000, SoPh, 193, 53
Klimchuk, J. A., Antiochos, S. K., Norton, D. 2000, ApJ, 542, 504
Klimchuk, J. A. 2015, Phil. Trans. R. Soc. A, 373, 20140256
Klimchuk, J. A., DeForest, C. E. 2020, ApJ, 900, 167
Kucera, T. A., Young, P. R., Klimchuk, J. A., DeForest, C. E. 2019, ApJ, 885, 7
Lemen, J. R., Title, A. M., Akin, D. J., et al. 2012, SoPh, 275, 17
López Fuentes, M. C., Klimchuk, J. A. 2006, ApJ, 639, 459
Malanushenko, A., Schrijver, C. J. 2013, ApJ, 775, 120
Figure 6. Panels A1 – A20 show the normalised Hi-C 2.1 intensities (blue), the AICc determined fit (red), and the Gaussian profiles (grey) generated to produce the fit for loop A. Emission is normalised with respect to the maximum peak intensity of panels A1 – A20. The Gaussian profiles are numbered in accordance with the bottom panel which shows the loop (black) and strand (cyan, magenta, and green) widths as a function of distance along the segment of the loop analysed. The error bars for the loop FWHM are ±1 Hi-C 2.1 pixel whereas the strand FWHM error bars are 5× the one-σ uncertainty returned from the curve fitting method. Note that Loop Position 0–25 Mm corresponds to south-to-north orientation in Figure 1.
Figure 7. Panels C1 – C12 show the normalised Hi-C 2.1 intensities (blue), the AICc determined fit (red), and the Gaussian profiles (grey) generated to produce the fit for loop C. Emission is normalised with respect to the maximum peak intensity of panels C1 – C12. The Gaussian profiles are numbered in accordance with the bottom panel which shows the loop (black) and strand (cyan, magenta, green, and orange) widths as a function of distance along the segment of the loop analysed. The error bars for the loop FWHM are ±1 Hi-C 2.1 pixel whereas the strand FWHM error bars are 5× the one-σ uncertainty returned from the curve fitting method. Note that Loop Position 0–17 Mm corresponds to south-to-north orientation in Figure 1.
Figure 8. Panels D1 – D11 show the normalised Hi-C 2.1 intensities (blue), the AICc determined fit (red), and the Gaussian profiles (grey) generated to produce the fit for loop D. Emission is normalised with respect to the maximum peak intensity of panels D1 – D11. The Gaussian profiles are numbered in accordance with the bottom panel which shows the loop (black) and strand (cyan, magenta, and green) widths as a function of distance along the segment of the loop analysed. The error bars for the loop FWHM are ±1 Hi-C 2.1 pixel whereas the strand FWHM error bars are 5× the one-σ uncertainty returned from the curve fitting method. Note that Loop Position 0 – 16 Mm corresponds to south-to-north orientation in Figure 1.
Figure 9. Panels E1–E10 show the normalised Hi-C 2.1 intensities (blue), the AICc determined fit (red), and the Gaussian profiles (grey) generated to produce the fit for loop E. Emission is normalised with respect to the maximum peak intensity of panels E1–E10. The Gaussian profiles are numbered in accordance with the bottom panel which shows the loop (black) and strand (cyan, magenta, and green) widths as a function of distance along the segment of the loop analysed. The error bars for the loop FWHM are ±1 Hi-C 2.1 pixel whereas the strand FWHM error bars are 5× the one-σ uncertainty returned from the curve fitting method. Note that Loop Position 0–18 Mm corresponds to north-to-south orientation in Figure 1.
Figure 10. Panels F1–F13 show the normalised Hi-C 2.1 intensities (blue), the AICc determined fit (red), and the Gaussian profiles (grey) generated to produce the fit for loop F. Emission is normalised with respect to the maximum peak intensity of panels F1–F13. The Gaussian profiles are numbered in accordance with the bottom panel which shows the loop (black) and strand (cyan, magenta, and green) widths as a function of distance along the segment of the loop analysed. The error bars for the loop FWHM are ±1 Hi-C 2.1 pixel whereas the strand FWHM error bars are 5× the one-σ uncertainty returned from the curve fitting method. Note that Loop Position 0–21 Mm corresponds to north-to-south orientation in Figure 1.
Figure 11. Panels G1 – G11 show the normalised Hi-C 2.1 intensities (blue), the AICc determined fit (red), and the Gaussian profiles (grey) generated to produce the fit for loop E. The Gaussian profiles are numbered in accordance with the bottom panel which shows the loop (black) and strand (cyan, magenta, and green) widths as a function of distance along the segment of the loop analysed. The error bars for the loop FWHM are ±1 Hi-C 2.1 pixel whereas the strand FWHM error bars are 5× the one-σ uncertainty returned from the curve fitting method. Note that Loop Position 0 – 12 Mm corresponds to north-to-south orientation in Figure 1.
Markwardt, C. B. 2009, Astronomical Data Analysis Software and Systems XVIII, 411, 251
McCarthy, M. I., Longcope, D. W., Malanushenko, A. 2021, ApJ, In Press
McClymont, Z., Mikic, Z. 1994, ApJ, 422, 899
Moré J. J. 1978, The Levenberg-Marquardt algorithm: Implementation and theory. In: Watson G.A. (eds) Numerical Analysis. Lecture Notes in Mathematics, vol 630. Springer, Berlin, Heidelberg.
Morgan, H., Druckmüller, M. 2014, SoPh, 289, 2945
Morton, R. J., McLaughlin, J. A. 2013, A&A, 553, L10
Nakariakov, V. M., Kosak, M. K., Kolotkov, D. Y., et al. 2019, ApJL, 874, 1
Parker, E. N. 1983, ApJ, 264, 642
Parker, E. N. 1988, ApJ, 330, 474
Peter, H., Bingert, S., Klimchuk, J. A., de Forest, C., Curtain, J. W., Golub, L., Winebarger, A. R., Kobayashi, K., Korreck, K. E. 2013, A&A, 556, A104
Pontin, D. I., Janvier, M., Tiwari, S. K., Galsgaard, K., Winebarger, A. R., Curtain, J. W. 2017, ApJ, 837, 108
Rachmeler, A. L., Winebarger, A. R., Savage, A. L., et al. 2019, SoPh, 294, 174
Scullion, E., Rouppe van der Voort, L., Wedemeyer, S., Antolin, P. 2014, ApJ, 797, 36
Watko, J., Klimchuk, J. A. 2000, SoPh, 193, 77
West, M., Zhukov, A., Klimchuk, J. A. 2014, COSPAR Scientific Assembly (Paris: COSPAR), E2.2-60-14
Williams, T., Walsh, R. W., Winebarger, A. R., et al. 2020a, ApJ, 892, 134
Williams, T., Walsh, R. W., Peter, H., et al. 2020b, ApJ, 902, 90
Yi L., Liu, Z., Wang, K., Chen, M., Peng, S., Zhao, W., He, J., Zhao, G. 2015, Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment, 775, pp 12-14