The disc-averaged star formation relation for Local Volume dwarf galaxies

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ABSTRACT
Spatially resolved H I studies of dwarf galaxies have provided a wealth of precision data. However these high-quality, resolved observations are only possible for handful of dwarf galaxies in the Local Volume. Future H I surveys are unlikely to improve the current situation. We therefore explore a method for estimating the surface density of the atomic gas from global H I parameters that are conversely widely available. We perform empirical tests using galaxies with resolved H I maps, and find that our approximation produces values for the surface density of atomic hydrogen within typically 0.5 dex of the true value. We apply this method to a sample of 147 galaxies drawn from modern near-infrared stellar photometric surveys. With this sample we confirm a strict correlation between the atomic gas surface density and the star formation rate surface density, which is vertically offset from the Kennicutt–Schmidt relation by a factor of 10−30, and significantly steeper than the classical \( N = 1.4 \) of Kennicutt (1998). We further infer the molecular fraction in the sample of low surface brightness, predominantly dwarf galaxies by assuming that the star formation relationship with molecular gas observed for spiral galaxies also holds in these galaxies, finding a molecular-to-atomic gas mass fraction within the range of 5–15 per cent. Comparison of the data to available models shows that a model in which the thermal pressure balances the vertical gravitational field captures better the shape of the \( \Sigma_{\text{SFR}}-\Sigma_{\text{gas}} \) relationship. However, such models fail to reproduce the data completely, suggesting that thermal pressure plays an important role in the discs of dwarf galaxies.

Key words: galaxies: dwarf – galaxies: irregular – galaxies: star formation – galaxies: structure.

1 INTRODUCTION
Star formation, the process by which gas is converted into stars, plays a central role in the evolution of a galaxy. Empirical constraints on the relationships between the present-day quantities of gas and star formation in galaxies may therefore form a crucial component in sub-grid recipes of hydrodynamic simulations and semi-analytical models (Fu et al. 2010; Lagos et al. 2011; Kuhlen et al. 2012; Popping, Somerville & Trager 2014; Furlong et al. 2015), which trace the formation of baryonic structures (galaxies) in dark matter haloes. Attempts to study the relationship between the gas and star formation rate (SFR) have been longstanding (Schmidt 1959), however only in modern times could any such relationship be demonstrated (Kennicutt 1998). In his pioneering study, Kennicutt (1998) found a strong correlation between the SFR surface density and the total gas surface density, fitting a power-law relation to a sample of spiral and starburst galaxies of the form,

\[
\Sigma_{\text{SFR}} = A \Sigma_{\text{Gas}}^{N}
\]

Power-law parametrizations of these quantities are referred to henceforth in this work simply as a star formation relation, or interchangeably, the Kennicutt–Schmidt relation (KS).

More recent studies achieved sufficient sensitivity and angular resolution to study the inner regions of Local Volume (d \( \lesssim 10 \) Mpc) spiral galaxies on kpc scales. These resolved studies instead demonstrated a strict correlation between the observed surface densities of molecular hydrogen \( H_2 \) and the SFR surface density whilst simultaneously demonstrating an anticorrelation with atomic hydrogen (HI)
above its saturation limit (Kennicut et al. 2007; Bigiel et al. 2008; Leroy et al. 2008). These studies indicated that the star formation relation was universal only when considering the molecular gas and not the total gas, for which the derived slope varied within and between galaxies. Indeed Krumholz, McKee & Tumlinson (2009b) successfully derived a universal local star formation relation, with significantly reduced scatter when considering a ‘free-fall’ time \( t_{ff} \).

\[
\Sigma_{SFR} = f_{H_2} \epsilon_{eff} \frac{S_H}{t_{ff}}
\]

where \( f_{H_2} \) is the fraction of the molecular gas and \( \epsilon_{eff} \) is a dimensionless star formation efficiency (SFE) scalefactor [see Krumholz (2014) for a recent review on the subject]. Further studies have challenged the universality of even the molecular star formation relation law (see discussions by Leroy et al. 2013b; Shetty et al. 2014). Comprehensive theoretical models should therefore accurately describe the observed distribution of apparent gas depletion times as a function of various environmental conditions or other factors and not just simply the surface densities of gas and star formation (SF). Comparing the agreement of the available data to theoretical models with varying underlying assumptions will therefore provide greater insight than just examining the linear regressions.

While in the inner discs of Local Volume spirals, the Hi content was not found to correlate with SFR surface density, the reverse is true in the outer Hi-dominated discs and low-mass late-type galaxies (Bigiel et al. 2010; Bolatto et al. 2011). Pushing \( H_2 \) column densities from \( 10 \, M_\odot \text{pc}^{-2} \) to \( 1 \, M_\odot \text{pc}^{-2} \), Bolatto et al. (2011) and Schruba et al. (2011) showed the molecular surface density is still correlated with the SFR surface density. These facts together imply that the molecular fraction in the Interstellar Medium (ISM) reaches a floor value of a few percent (Krumholz 2013). Ostriker, McKee & Leroy (2010) and Krumholz (2013) developed theoretical models in order to describe the levels of star formation observed in the Hi-dominated regime, with varying degrees of success. The Krumholz (2013) model successfully describes the outer discs of spirals and dwarf galaxies (Koribalski & López-Sánchez 2009; Bigiel et al. 2010; Bolatto et al. 2011). However, for disc-averaged quantities derived from dwarf galaxies (Wyder et al. 2009; Roychowdhury et al. 2014) and the resolved Roychowdhury et al. (2015) data set, the Ostriker et al. (2010) model provides a better agreement. A key difference between the two models is that Krumholz (2013) includes the effect of gas metallicity on the transition from atomic to molecular hydrogen, which is inspired by the premise that \( H_2 \) forms on the surface of dust grains. The Ostriker et al. (2010) model does not consider the chemical state of the gas, but only its thermodynamic state by imposing pressure balance between the different ISM phases. With different underlying theoretical assumptions, distinguishing between these two models will provide important insight into the processes that govern star formation in H\text{-}dominated environments.

While resolved studies of dwarf galaxies have provided a wealth of precision data, taken together, these studies (Bigiel et al. 2010; Roychowdhury et al. 2015) were constrained to only 27 dwarf galaxies of the 107 observed by Begum et al. (2008) and Hunter et al. (2012) compared to the \( \sim 400 \) irregular galaxies in the Local Volume. Future HI surveys, whilst very sensitive, are unlikely to resolve anything but the nearest dwarf galaxies (Koribalski 2008, 2012). Despite this, multwavelength coverage of dwarf galaxies in the Local Volume is particularly good (see Karachentsev, Makarov & Kaisina 2013, and references therein), often only the Hi resolution is lacking. In order to increase the sample size to include dwarfs at greater distances, we must find approximate methods for computing the surface gas density. In this work, we provide a procedure for approximating the surface density of the gas from global Hi parameters and precision stellar photometry. We test the accuracy of our method by using the Wyder et al. (2009) and Kennicutt et al. (1998) galaxies as control samples.

This paper is organized as follows: In Section 2 we describe the galaxy samples, catalogues, and our computed parameters. In Section 3 we present our results, analysis, and discussion. Particularly, we describe the accuracy of our gas surface density estimation. We then compare our data to resolved observations. Although vertically offset from spiral galaxies, we show that low surface brightness galaxies (LSB) follow a similar distribution. Considering only the vertical offset and assuming a constant time-scale to convert the \( H_2 \) into star formation, we provide an estimation of a typical molecular fraction. In Section 4 we compare all the available data in the literature to various models. Finally, we conclude in Section 5.

2 METHODOLOGY

2.1 Samples

To study the star formation relation (from here on we use the phrases star formation relation and the KS relation interchangeably) in a comprehensive sample of Local Volume dwarfs (\( M_\star < 9 \, M_\odot \)), low-mass late-type and LSB galaxies, we employ data from various sources in the literature that we describe next.

2.1.1 Near-infrared photometry

The global disc-averaged quantities used in the KS relation are typically computed from some fiducial radius corrected for inclination that is ideally representative of the star-forming disc. The choice of radius has not remained consistent over time. The K98 sample parameters were computed using the ‘RC2 radius’, the B-band 25th surface brightness isophotal diameters from the second reference catalogue (i.e. \( D_{25} \), de Vaucouleurs et al. 1991; Bremnes, Binggeli & Prugniel 1998, 1999, 2000; Jerjen, Binggeli & Freeman 2000; Barazza, Binggeli & Prugniel 2001; Parodi, Barazza & Binggeli 2002; Makarova et al. 2005) were typically conducted in the optical regime and thus definitions of the stellar and star-forming discs naturally followed from B-band photometry. Improvements in charge-coupled device (CCD) technology and the introduction of near-infrared (NIR) detectors have since resulted in accurate JHKs photometry of Local Volume galaxies (Noeske et al. 2003; Vaduvescu et al. 2005; Vaduvescu, Richer & McCaill 2006; Kirby et al. 2008; Vaduvescu & McCaill 2008; Fingerhut et al. 2010; de Swardt, Knaan-Korteweg & Jerjen 2010; McCall et al. 2012; Young et al. 2014). In cases where the integration times are sufficient to overcome the bright sky background, the NIR offers several advantages over the optical when determining geometric properties of the stellar disc. It is significantly less sensitive to dust that will invariably attenuate and distort the flux (Driver et al. 2007) and in addition the NIR flux contribution of the young stellar population is only significant in moderately strong starbursts (Krueger, Fritz & Alvesleben & Loose 1995). Irregularities in morphology such as randomly distributed H\text{ii} regions and associated H\text{a} emission are therefore less...
significant, allowing a greater accuracy in determining the stellar galactic center (and the resulting ellipse) that might have otherwise been centered on an offset H$_2$ region.

When computing the parameters required for the KS relation, determinations of the disc radius employ the surface photometry from recent NIR Studies (Kirby et al. 2008; McCall et al. 2012; Young et al. 2014, hereafter YJLK14, MVPB12, KRDJ08, respectively), which have precisely measured the stellar discs of various Local Volume galaxies, mostly consisting of dwarf irregulars, low-mass late-type, and blue compact dwarf galaxies. Using NIR surface photometry is unusual in the sense that we could simply use the Holmberg diameters from Lauberts & Valentijn (1989) and de Vaucouleurs et al. (1991). It is expected that the ‘equivalent’ Holmberg radii in the NIR will still be more accurate, despite requiring the B-band magnitude to compute this parameter (see Section 2.2.3), for the reasons listed above.

In this study, the samples of YJLK14 and KRDJ08 are amalgamated to form the primary sample of galaxies since we have full access to their data and computed parameters. Together they form a sample of 79 galaxies with several properties. First, a morphology that ranges from some low-mass ellipticals and high-mass lenticulars to many low-mass late types and dwarf irregulars. A broad range in stellar mass, 6.5 < log$_{10}(M_*/M_\odot)$ < 11, with a sample median of 8.3. This sample is mostly dominated by low-mass late-type galaxies and dwarf irregulars. Finally, the KJRD08 and YJLK14 samples conveniently trace the main cosmic structures of the Southern hemisphere out to 10 Mpc (the Sculptor and Cen A group, respectively).

To further supplement the YJLK14 and KRDJ08 samples, we also source data from the MVPB12 study. This is an amalgamated K$_s$-band data set of newly observed galaxies and previous photometric studies filtered to include only those galaxies for which a surface brightness profile was successfully fitted, and for which the tip studies filtered to include only those galaxies for which a surface band data set of newly observed galaxies and previous photometric McCall (2008, 17 galaxies), and Fingerhut et al. (2010, 80 galaxies).

In ideal circumstances, suitably resolved H I data of dwarf irregulars would be used to measure the gas densities point by point, and compared to the associated SFR surface density as has been conducted in the studies of Bigiel et al. (2008) and Roychowdhury et al. (2015). For dwarf galaxies, sensitivity and angular resolution of the HI maps can be a particularly constraining factor (although the availability of SFR tracers may be an equally constraining factor), and so other previous studies have measured surface densities averaged over the entire star-forming disc (Wyder et al. 2009; Roychowdhury et al. 2014). Most galaxies in the YJLK14, KRDJ08, and MVPB12 samples described above do not have readily available resolved HI maps. In order to increase the statistics of dwarf galaxies in the make up of the star formation relation diagram, we resort to deriving the atomic gas density from the available total HI fluxes, averaged within the geometric parameters derived from the NIR photometric samples.

We obtain HI fluxes, with a few exceptions, from the HI Parkes All-Sky Survey (HIPASS) catalogues of Koribalski et al. (2004) (1000 Brightest Galaxy Catalog) and Meyer et al. (2004). The HIPASS sample was observed on the 64m Parkes radio telescope using the 21cm multibeam receiver, a correlator bandwidth of 64 MHz divided into 1024 channels, and beam-width of ∼15 arcmin (Staveley-Smith et al. 1996). The MVPB12 study has already compiled HI fluxes for their galaxies from other sources (see their Table 4) and we simply adopt their values for those galaxies. For other galaxies we have obtained HI data from either the Bouchard et al. (2005) or Begum et al. [2008, Faint Irregular Galaxies GMRT Survey (FIGGS)] study.

It is possible that the derived gas surface densities would introduce a bias and slope offset in the data which will require correction. Potential statistical biases resulting from this estimation is explored in Section 3.1.

2.1.2 HI fluxes, gas densities

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2.1.3 UV and 24µm fluxes, SFR tracers

Studies comparing the SFR estimates derived from H$\alpha$ and UV fluxes for Local Volume galaxies have found fundamental discrepancies where in principle it is expected they should agree (Lee et al. 2009; Meurer et al. 2009; Karachentsev & Kaisina 2013). H$\alpha$ flux is systematically lower relative to the Far-Ultraviolet (FUV) with decreasing luminosity, underestimating the flux relative to the FUV by up to an order of magnitude. One explanation, as Meurer et al. (2009) suggest, is that variations in the initial mass function (IMF) of low-luminosity galaxies are responsible. This follows logically from the relative sensitivities of each tracer with respect to the IMF. H$\alpha$ emission resulting from ionization of the surrounding ISM will require stars in excess of 15 M$\odot$ whose ionizing flux is sufficiently strong. In contrast, ultraviolet emissions directly trace the photonic emissions of stars of several solar masses (Kennicutt & Evans 2012). Other works by Fumagalli, da Silva & Krumholz (2011), and Weisz et al. (2012) instead suggest temporal variation in the SFRs as the cause. The above-mentioned stochastic effects pronounce the gap between the underlying and traced SFR, appear to affect H$\alpha$ more significantly than FUV (da Silva, Fumagalli & Krumholz 2014; Roychowdhury et al. 2014). We therefore elect to use FUV fluxes when computing the SFR surface density.

As part of the 11Mpc H$\alpha$ and Ultraviolet Galaxy (11HUGS) survey, Lee et al. (2011) presented UV photometry of a complete sample of Local Volume galaxies. We cross-correlate galaxies within the primary sample and MVPB12, extracting where available observed total FUV fluxes. In instances when a total FUV flux is not available, we instead use the aperture flux, defined as the aperture beyond which the flux error becomes 0.8 mag or where the intensity falls below the sky background level. Statistically, systematic differences between the aperture and total fluxes are negligible as shown in Fig. 1, especially when compared to other sources of systematic errors.

The major drawback of using the FUV flux is its sensitivity to dust absorption. A composite tracer (Hao et al. 2011) accounting for the stellar emission re-radiated in the infrared via dust will therefore provide a better estimate of the SFR, although it is expected that for our sample dominated by low-metallicity dwarf galaxies, these corrections should be small. The Local Volume Legacy survey (Dale et al. 2009) is a legacy Spitzer Space Telescope volume limited survey designed to complement the 11HUGS and ACS Nearby Galaxy Survey Treasury (Dalcanton et al. 2009) with observations of the near, mid, and infrared fluxes of nearby galaxies. Using the 24 µm fluxes, we are able to correct our SFR tracer dust extinction
in \( \sim 35 \) per cent of our galaxies (for median change in the measured SFR of 0.04 dex).

2.2 Derived parameters

In the following subsections we describe the methods used to obtain the SFR surface density and the atomic gas surface density. Table 1 compiles the sample-observed properties while Table 2 lists the derived properties.

2.2.1 Estimating the SFR

For estimating the FUV-traced SFR, we first correct the available asymptotic magnitude for Galactic extinction (Schlafly \\& Finkbeiner 2011) using the relation given by Karachentsev et al. (2013),

\[
m_{\text{FUV}} = m_{\text{FUV}} - 1.93 \left( A_B^G + A_B^I \right)
\]

where \( A_B^G \) and \( A_B^I \) are the Galactic and internal extinction corrections, respectively, in the \( B \)-band. We make no attempts to correct for internal extinction at this stage, since we account for internal extinction later using the 24 \( \mu m \) flux. The FUV flux density \( f_i \) is computed from the total FUV magnitude \( m_{\text{FUV},0} \) given in Column 7 of Table 1,

\[
f_i(\text{erg s}^{-1} \text{ cm}^{-2} \text{ Hz}^{-1}) = 10^{-0.4(m_{\text{FUV},0}+48.6)}.
\]

Using the best available distances in the literature (Column 5 in Table 1) and the flux densities, we compute the FUV and 24 \( \mu m \) luminosities \( L \),

\[
L = v f_i \times 4\pi D^2.
\]

For a constant SFR over 100 Myr, solar metallicity and either a Salpeter (Salpeter 1955) or a Kroupa IMF (Kroupa 2001), the attenuation-corrected FUV luminosity, \( L(\text{FUV})_{\text{corr}} \) (Column 2 in Table 2), is given by Hao et al. (2011):

\[
L(\text{FUV}, \text{corr}) = L(\text{FUV}) + 3.89L(25\mu m).
\]

The Hao et al. (2011) recipe was derived using the Infrared Astronomical Satellite (IRAS) 25\( \mu m \) observations. We instead use the Spitzer 24\( \mu m \) flux (Column 8 in Table 1), which introduces an uncertainty of less than 0.3 mag (Hao et al. 2011) due to the systematically lower luminosities recovered by IRAS observations (Kennicutt et al. 2009, Fig. 1) relative to Spitzer. Galaxies in the YJLK14, MVPB12, and KRDJ08 samples without a 24\( \mu m \) flux have their values estimated using the following relationship as a zeroth-order approximation.

\[
\log_{10} L(24\mu m) = 1.11^{+0.09}_{-0.09} \log_{10} \frac{M_*}{[M_\odot]} + 31.415^{+0.739}_{-0.739}
\]

derived from the least squares regression of the galaxies with available 24 \( \mu m \) flux measurements as shown in Fig. 2. As demonstrated, the 2\( \sigma \) trends provided reasonable upper and lower bound limits to the available data. We have conservatively elected to use the lower bound relationship to correct for dust since it is plausible that many dwarf galaxies in the sample have inconsequential dust content. We note that dust measurements remain a large source of uncertainty for those galaxies without a 24\( \mu m \) flux measurement, since the data are scattered over approximately two orders of magnitude.

Plugging the corrected FUV luminosity into the recipes prescribed by Hao et al. (2011) and Kennicutt \\& Evans (2012) we obtain the SFR \( (M_* \text{ yr}^{-1}) \) (Column 3, Table 2),

\[
\log_{10} \frac{M_*}{[M_\odot \text{ yr}^{-1}]} = \log_{10} \frac{L(\text{FUV}, \text{corr})}{[\text{erg s}^{-1}]} - 43.35
\]

As to be expected for the dwarf and LSB galaxies, dust corrections to the SFRs are typically low. The median change in the measured SFR is 0.04 dex although a maximum of 0.5 dex is recorded indicating the importance of dust corrections in the case of some galaxies.

SFR values from Kennicutt (1998) and Wyder et al. (2009) require a correction \( (M_* = 0.63M_{*,K_0}) \) to account for updated stellar population models and the choice of IMF used in more modern studies. We have performed this correction in the analysis to bring them into line with more modern studies.

We calculate the uncertainty in the measurements by including the uncertainty in distance (typically between \( \pm 10 \)–20 per cent), the flux, and the errors in the calibration. To get total errors, we add these uncertainties in quadrature. In all the figures we show representative error bars that were calculated as the average error on the quantities of the galaxies shown.

2.2.2 HI and gas mass estimation

We estimate the HI mass (compiled in Column 4, Table 2) for our sample galaxies following Roberts (1975),

\[
M_{\text{HI}} = 2.36 \times 10^5 D^2 F_{\text{HI}},
\]

where \( D \) is the distance of the galaxy from the sun and \( F_{\text{HI}} \) is the 21 cm emission line flux (Column 9, Table 1). The dwarf and low-mass late-type galaxies are assumed to have a negligible molecular fraction and so the total gas mass \( M_{\text{gas}} \) is simply the HI mass corrected for the presence of helium using a factor of 1.34.

2.2.3 Geometric and density computations

In order to find the NIR equivalent Holmberg radius \( R_{26.5, eq} \), we use the extinction-corrected \( (B-H)_{0} \) and \( (B-Ks)_{0} \) colours. YJLK14 demonstrated (their Figure 10) significant variation in the colours of...
Table 1. Table listing the externally obtained properties required to compute the surface densities for the KRDJ08 and YJLK14 NIR samples. The table is arranged as follows: Column 1 – Galaxy name; Columns 2 and 3 – RA and DEC; Columns 4 – Morphology, using the classification scheme by de Vaucouleurs et al. (1991); Columns 5 and 6 – the radial distance in Mpc and the derivation method, respectively. Note that the obtained values have been rounded to the nearest decimal place since distance derivation methods are typically no more accurate than 10 per cent; Column 7 – FUV flux; Column 8 – the 24 μm luminosity; Column 9 – the H I flux; Column 10 – the B-band galactic extinction; Column 11 – the total observed luminosity in the B-band; Column 12 – B − H colour corrected for extinction (or the B−Ks data for the MVPB12 sample). Quantities are carefully cited in the caption for the KRDJ08 and YJLK14 samples. For the MVPB12 sample, their values have been taken as and when available (such as distance modulus, H I fluxes, extinctions etc). The authors did not, however, compile a list of B-band magnitudes, which we require in our computation of R_{26.5, eq}. Instead, we obtained them using the de Vaucouleurs et al. (1991) RC3 catalogue. Similarly, the quantities calculated for Kennicutt (1998) and Tully & Fisher (1988) cross-correlated galaxies are not presented but these data can be made available upon request.

References: (a) Karachentsev et al. (2002a), (b) Karachentsev et al. (2003b), (c) Karachentsev et al. (2006), (d) Karachentsev et al. (2007), (e) Karachentsev et al. (2013), (f) Tully et al. (2008), (g) Tully et al. (2008a), (i) Karachentsev et al. (2002b), (j) Karachentsev et al. (2000), (k) Seth, Dalcanton & de Jong (2005), (l) Roychowdhury et al. (2012), (m) Cannon et al. (2003), (n) Grisé et al. (2008), (o) Tosi et al. (2001), (p) Tully et al. (2001), (q) Dalcanton et al. (2009); U−V-band (a) GALEX, (b) Lee et al. (2011); B−band (a) de Vaucouleurs et al. (1991), (b) Lauberts & Valentijn (1989), (c) Karachentsev et al. (2013), (d) Metcalfe, Godwin & Peach (1994), (e) Parodi et al. (2002), (f) Jerjen et al. (2000), (g) Warren, Jerjen & Koribalski (2007), (h) Karachentsev et al. (2004), (i) Warren, Jerjen & Koribalski (2006), (j) Kouwenhoven et al. (2007), (k) Roychowdhury et al. (2012); H I FluX. (a) Doyle et al. (2005), (b) Begum et al. (2008), (c) Bouchard et al. (2005). For references pertaining to the MVPB12 data, the reader should consult their study.

Table 2. Table listing the quantities used to obtain the NIR catalogue galaxies, and is arranged as follows: Column 1 – Name, Column 2 – L(FUV)_{corr}, Column 3 – M_{B, eq}, Column 4 – M_{HI}, Column 5 – R_{26.5, eq}, Column 6 – Σ_{HI}, Column 7 – Σ_{SFR}.

For the amalgamated MVPB12 sample, all parameters are generated using the semimajor axis as the native radial coordinate and so no further corrections are required to compute the area of the disc defined by the semimajor axis. The KRDJ08 and YJLK14 dwarf galaxies and thus it is important to perform colour corrections directly rather than through the use of a scaling relationship.

The NIR equivalent Holmberg radius (R_{26.5, eq}) for the primary sample is computed from equation (1) in YJLK14 and is given by

\[ R_{26.5, eq} = [0.921(26.5 - [(B - H)_{eq}]) - 0.921H_{0}]^{1/2} r_0, \]

where \( \mu_0 \) is the central surface brightness in the H-band, \( n \) is the Sérsic index, and \( r_0 \) is the scalelength parameter in units of pc. Similarly, following from equation (1) in MVPB12,

\[ R_{26.5, eq} = \text{acosh} \left[ 10^{(-0.4\mu_0 - (26.5 - [(B - Ks)_{eq}])]} \right] r_0. \]

For the amalgamated MVPB12 sample, all parameters are generated using the semimajor axis as the native radial coordinate and so no further corrections are required to compute the area of the disc defined by the semimajor axis. The KRDJ08 and YJLK14 data were instead computed using the geometric mean radius. The area defined by the semimajor axial component of the R_{26.5, eq} in this case is,

\[ A = 2\pi R_{26.5, eq}^2 (1 - e), \]

where \( e \) is the measured ellipticity. The estimated SFRs and H I masses are averaged over this quantity to derive an estimate of the atomic gas and SFR surface densities for the NIR galaxy samples. Along with R_{26.5, eq}, the quantities are compiled in Table 2. The Tully & Fisher (1988) catalogue include an inclination-corrected Holmberg diameter and it is therefore trivial to calculate the atomic gas and SFR surface densities.
3 RESULTS AND DISCUSSION

The main focus of the following discussions is to investigate the trends in the star formation relation in the H I-dominated regime. Noting the limitations a linear model poses on an obviously multi-dimensional problem, a later section is dedicated to comparing the gathered data to various comprehensive models of star formation.

3.1 How accurate is \( M_{\text{HI}} / A \) as a proxy for \( \Sigma_{\text{gas}} \)?

Before proceeding, we must ensure that \( M_{\text{HI}} / A \) is a valid proxy for \( \Sigma_{\text{gas}} \). The apparent correlation and linearity between the total atomic gas and the SFR as shown in Fig. 3 suggest this might be the case. Dwarf galaxies show a very consistent and linear relationship over a broad range of \( \text{HI} \) masses. The linearity of this relationship suggests that by normalizing to a fiducial disc area, such as that defined by the Holmberg diameter, we do not introduce a secondary effect on the measured slope of the linear regression to the data points. Of course, we may introduce a bias and an offset in the \( \Sigma_{\text{gas}} \) scale since using the \( M_{\text{HI}} / A \) proxy we are insensitive to variation in the ratio of the optical-\( \text{HI} \) diameter (\( A \) is derived following the optical data).

In order to determine the typical value by which we over or underestimate the actual gas surface density, we calculate \( M_{\text{HI}} / A \) for the spiral galaxies from K98, and the dwarf galaxies from Wyder et al. (2009) and Roychowdhury et al. (2014) comparing them to the \( \Sigma_{\text{gas}} \) calculated in the respective studies. As mentioned previously, we obtain global \( \text{HI} \) fluxes, inclinations, and isophotal radii for the K98 galaxies from the Nearby Galaxy Atlas catalogue. For the LSB galaxies, these quantities are obtained from the RC3 catalogue and for the Roychowdhury et al. (2014) these are obtained from Begum et al. (2008). Fig. 4 plots the surface gas densities against the computed \( M_{\text{HI}} / A \) quantities. We emphasize \( A \) has been derived here not using the \( \text{HI} \) data but the optical data, i.e. considering the Holmberg radius and adding the factor \( 1/\cos i \) to include the geometric correction (see YJLS14). As shown in the plot, most data points are scattered around unity typically within 0.5 dex. There is an obvious trend from overestimation to underestimation with increasing \( \text{HI} \) mass. Fortunately this bias appears to be linear and we correct for it using a least squares approach. The Pearson correlation coefficient of this fit is \( r = 0.750 \). We derive the correction

\[
\log_{10} \Sigma_{\text{HI}} = (0.4 \pm 0.1) \log_{10}(M_{\text{HI}}/A_{26.5}) + (0.38 \pm 0.04),
\]
Figure 5. Surface density of the SFR as a function of the gas surface density for the LSB galaxies obtained from the NIR samples, KRDJ08, YJLK14, and MVPB12 and whose atomic gas surface densities have been estimated from global parameters as outlined in Section 2. Dashed lines correspond to slopes of constant gas depletion times in units of years, as labelled. The solid black line corresponds to the best-fit obtained using HYPER-FIT (Robotham & Obreschkow 2015), adopting the conjugate gradients method. The dotted lines mark the 1σ uncertainty in the zero-point of the relation. The cross in the bottom right of the panel shows a representative error bar of individual measurements.

Figure 6. The Kennicutt–Schmidt relation for YJLK14, MVPB12, and KRDJ08 (open circles) sample galaxies compared to the original K98 data (plus symbols for spirals, crosses for starbursts). Additionally, we have included the disc-averaged quantities for the galaxies whose column densities were measured directly (Wyder et al. 2009; Roychowdhury et al. 2014, black triangles). The open and filled stars with errorbars show the median and 1σ scatter of the spiral outskirts and dwarf galaxies of Bigiel et al. (2010), respectively, both of which correspond to HI-dominated regions. For clarity, we artificially displaced the medians of the dwarf galaxies by 0.04 dex in the x-axis. The Roychowdhury et al. (2015) data for their ‘THINGS 1kpc’ (orange circles), ‘FIGGS 400pc’ (blue circles), and ‘Bluediscs main’ (green circles) samples are also shown for comparison. The K98 galaxies have been corrected for the presence of helium contrary to the original work. The diagonal dashed lines corresponds to slopes of constant gas depletion times in units of years, as labelled. The solid line shows the best fit to selected data, as described in the text, using the same the procedure described in Fig. 5. The cross in the bottom right of the panel shows a representative error bar of individual measurements.

3.2 The Kennicutt–Schmidt relation for Local Volume galaxies

Using the data and derived parameters described in Section 2, we plot the gas and SFR surface densities. Fig. 5 explores the simple linear regression to the SFR relation for LSB galaxies from KRDJ08, YJLK14, and MVPB12. Fig. 6 extends the regression analysis to include LSB galaxies and spiral galaxies from further sources (Kennicutt 1998; Wyder et al. 2009; Roychowdhury et al. 2014) whilst the outer disc (Bigiel et al. 2010; Roychowdhury et al. 2015) and starburst data (Kennicutt 1998) are included in the plot for comparative purposes only. In order to obtain a best fit to our data and quantify the power-law index of the relation $\Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}}^n$, we use the HYPER-FIT R-package of Robotham & Obreschkow (2015). We perform the fits using the Optim algorithm with the conjugate gradients method, minimising the scatter orthogonal to the plane. In the fit we included the errorbars for individual objects, and assume that the errors in the x and y axis are not correlated. The best fit obtained for the LSB galaxies from KRDJ08, YJLK14, and MVPB12 is

$$\log_{10} \Sigma_{\text{SFR,LSB}} = 2.19^{+0.25}_{-0.21} \log_{10} \Sigma_{\text{gas}} - 4.96^{+0.22}_{-0.22}$$

including all the data as outlined above, the corresponding best-fitting relation is instead,

$$\log_{10} \Sigma_{\text{SFR,spirals and LSB}} = 1.97^{+0.11}_{-0.09} \log_{10} \Sigma_{\text{H}} + H_2 = 4.77^{+0.28}_{-0.28}$$

Fig. 5 shows that there is a clear correlation between the surface densities of the SFR and the atomic gas with a steep dependence on the latter quantity. Although we did not include the Bigiel et al. (2010) data in the least squares fit shown in Fig. 6, visual comparison of their data set to the line of best fit seems to show a good agreement, although we remind that the Bigiel et al. (2010) points have too high depletion time. We note, however, the narrow range in $\Sigma_{\text{H}}$ for our sample galaxies, which spans from 0.2 to 1.2 in a log scale in Fig. 4. This is a consequence of the fit to the data from Wyder et al. (2009) and Roychowdhury et al. (2014) samples that we apply to the unresolved HI data. Possible biases in the samples, for example by being sensitive to only a narrow range in $\Sigma_{\text{SFR}}$ or $\Sigma_{\text{H}}$ (unlike the spiral galaxies from Kennicutt 1998, which span a much wider range in both axes), could lead to the data preferring an $N=1$ slope due to the reduced dynamic range. If this were the case,
using resolved HI data to estimate HI distributions could change our results.

The slopes derived for the LSB galaxies in our study are much steeper than that found in Roychowdhury et al. (2014) and is more supportive of the findings of Roychowdhury et al. (2015). Roychowdhury et al. (2015) suggested this difference could be an effect of being biased towards the inner star-forming regions of galaxies. If that were the case, we might expect the same phenomenon in our sample galaxies that are also disc-averaged quantities. Instead they form a tight distribution intermediate to the outer disc data of Bigiel et al. (2010) and the spirals of Kennicutt (1998). Indeed, we note that the two determinations of the KS relation slope (1.97 for the combined spirals+LSB sample and 2.19 for the LSB sample) agree within the fitting errors. Therefore, using the LSB sample we are probably circumventing any existing bias (as the mentioned narrow range in $\Sigma_{HI}$ in the Wyder et al. (2009) and Roychowdhury et al. (2014) samples and reinforcing the results obtained by Kennicutt (1998).

Our sample includes galaxies over a much wider range of surface brightness than the sample of Roychowdhury et al. (2014): LSB galaxies from YJK14, the somewhat brighter low-mass late types and irregulars from KRDJ08, as well as star-forming dwarfs and additional LSB galaxies from the amalgamated MVPB12 sample. We suggest that $N=1$ slope would be simply due to insufficient statistics especially given the generally good agreement between the Wyder et al. (2009), Roychowdhury et al. (2014), the novel KRDJ08, YJK14, and MVPB12 data sets. For dwarf galaxies, we find a slope that is strictly not in agreement with the canonical $N=1.4$ derived from the original K98 sample. As Bigiel et al. (2008) noted, the $N=1.4$ relies on the contrast of spiral discs and the molecular rich circumnuclear starbursts.

Notably, the galaxy NGC 1569 (labelled in Fig. 6) lies well outside the expected behavior for spirals or dwarf galaxies. Environmental interactions resulting in the star-burst activity are very likely to be the cause of NGC 1569 significant offset from the star formation relation with respect to the broader population of galaxies (e.g. Mühle et al. 2000), as also discussed in the case of NGC 5253 (López-Sánchez 2010; López-Sánchez et al. 2012).

3.3 Comparing global and resolved properties

Above the critical density of the total gas ($\sim 9 \, \text{M}_\odot \, \text{pc}^{-2}$), in the $\text{H}_2$-dominated regions of their spiral galaxies, Bigiel et al. (2008) and Leroy et al. (2013) found a universal molecular star formation relation with a corresponding exponent of $N=1$. Conversely, when looking at the corresponding total gas or HI gas star formation density diagrams, exponents are found to vary significantly radially within galaxies and from galaxy to galaxy. Above the critical density, the atomic gas saturates in these galaxies and there is no observed correlation between the atomic or total gas with the SFR. While, below the critical density where the gas is HI-dominated, the atomic gas and SFR surface densities correlate (Koribalski & López-Sánchez 2009; Bigiel et al. 2010; Bolatto et al. 2011; López-Sánchez et al. 2015). This relationship does not have a fixed slope.

Variation of the total gas SFR relations implies that the ratio of HI-to-$\text{H}_2$ can vary within galaxies and in between galaxies, or rather that the SFE is not constant due to either local or global factors. More recent work has confirmed significant variation of the SFE between different THINGS galaxies (Shetty et al. 2014), but they studied the molecular hydrogen. While factors other than the surface density of the gas have been shown to influence the SFE, in their sample, Leroy et al. (2008) demonstrated where the ISM is dominated by atomic gas, such as in the outer disc of spirals, the SFE decreases with increasing radius, implicating a global radial dependence on SFE in addition to local variation. The studies of Elmegreen & Hunter (2015) and Roychowdhury et al. (2015) provide further evidence for radial dependence on the SFE.

Recently Wang et al. (2017) used high-quality interferometric HI data from the LVHIS (Local Volume HI Survey, Koribalski et al. 2018), including a multiwavelength data set that allows to perform a careful estimation of the SFR, to find that the correlation between the globally averaged $\Sigma_{SFR}$ and $\Sigma_{HI}$ is weak. Their figure 11 shows these data; their galaxies seem to overlap on the scatter from our Fig. 6. They also found that the SFE significantly depends on the average stellar surface density, something that can be explained using a marginally stable disc model, as described in Wong et al. (2016). This was already explored by Shi et al. (2011), who proposed an explicit dependence of the SFE on the stellar mass surface density (the ‘extended Schmidt law’). The SFE–$\Sigma_{disc}$ relation proposed by Shi et al. (2011), which can be reproduced by some models and holds over five orders of magnitude in $\Sigma_{disc}$ for individual global galaxies, included LSB and dwarf galaxies that deviate from the KS law.

With the increase in sample size relative to prior studies, we are able to reproduce similar trends shown in resolved studies and reconcile some of the inconsistency introduced by Roychowdhury et al. (2014). Both resolved and disc-averaged studies imply a ‘floor’ on the fraction of $\text{H}_2$ gas given the shape of the distributions in Fig. 6. The resolved and disc-averaged data are not in complete agreement when it comes to the slope of the star formation relationship. Bigiel et al. (2010) and Roychowdhury et al. (2015) find exponents on average of $N=1.5$, while this study finds a much steeper slope ($N=2.4$) for the disc-averaged data, albeit with a large uncertainty. This statistical uncertainty in the slope greatly decreases when including the spiral disc data from Kennicutt (1998) and this is reflected in the correlation coefficients of these fits increasing from $r = 0.670$ to 0.795.

Roychowdhury et al. (2015) suggested that this apparent inconsistency arises from the bias when looking at optical disc-averaged quantities. It is possible to imagine resolved regions within an HI disc with similar gas surface densities to a disc-averaged value for a given galaxy but with little or no star formation as they may lie outside the star forming disc. One potential means of resolving this inconsistency is to use the total area of the HI disc rather than the optical disc. This would require a trend in the optical to HI diameter such that galaxies with higher surface densities had a larger diameter ratio relative to galaxies with lower surface densities.

Ultimately as the distribution of points in Fig. 6 demonstrates, the star formation relationship is more complex than what linear relationships would imply. We note that our data occupy a narrow range of atomic surface densities, while the numerous resolved data points from Bigiel et al. (2010) occupy a much wider range and show a complex distribution. Within this distribution itself significant variation of the exponent of the star formation law is easily possible. We suggest that such variations in slope are an indicator of the complexity of the problem and that a more nuanced approach would be required to fully describe the distribution of the data. Section 4 describes the available comprehensive models dealing with the star formation relationship and compares the available data to them in order to obtain greater insight.
3.4 Physical causes for the variation in the SFE

At least some of the scatter, and therefore the overall offsets in the distribution of the Local Volume galaxies, particularly the dwarfs, must occur from variations in the scaleheight of the disc. Schmidt (1959) originally proposed that $\rho_{\text{SFR}} \sim (\rho_{\text{gas}})^p$, where $\rho_{\text{SFR}}$ and $\rho_{\text{gas}}$ are the SFR and gas volume densities, respectively. For constant scaleheights, such as in ideal spirals whose intrinsic axial ratio is well known ($\sim 0.2$), projection effects play no part in the variation of SFE. There is evidence that Local Volume galaxies and dwarfs do not have a constant scaleheight (Roychowdhury et al. 2010, 2013).

Modeling a galaxy’s stellar discs as triaxial ellipsoids, Roychowdhury et al. (2013) used Monte Carlo simulations to determine the minor ($q$) and major ($p$) intrinsic axial ratios of irregular galaxies of the Local Volume. These galaxies demonstrated a significant degree of variation in their intrinsic axial ratios $0 < q_0 < 1$, which was mildly correlated with luminosity. Perhaps, of more relevance to this study is the intrinsic axial ratio of the gas distribution. For a sample of faint dwarf irregulars from the FIGGS sample, Roychowdhury et al. (2010) determined a mean axial ratio of $⟨q⟩ = 0.6$ for their sample. Note, however, that the axial ratio of $⟨q⟩$ provided by Roychowdhury et al. (2010) had a large associated error, and therefore a large intrinsic variation in the ratio from galaxy to galaxy is expected.

Assuming a disc in which the gas volume density decays exponentially, the surface density $\Sigma_{\text{gas}}$, and central volume density $\rho_{0,\text{gas}}$ are related by the scaleheight as $\rho_{0,\text{gas}} = \Sigma_{\text{gas}}(2h)$. As in the LSB galaxies in the Wyder et al. (2009) and the Roychowdhury et al. (2014) sample, the Local Volume galaxies in this study also display a factor $\sim 5$ offset in gas depletion times to the spiral in the original K98 sample, which if entirely attributable to changes in scaleheight, would imply that late type and irregular galaxies have discs with significantly larger scaleheights relative to spiral galaxies.

Relatively speaking, potentially thicker disc scaleheights in dwarf irregulars would lead to a lower effective volume density, increased free-fall time and thus lower observed SFE. Indeed in their study of 20 dwarf irregular galaxies, Elmegreen & Hunter (2015) considered the effects of disc thickness extensively. The dwarf galaxies in their sample were shown to be thick in absolute terms, with gas scaleheights of 0.5 kpc and a typical ratio of scaleheight to radius of 0.6. Remarkably, correcting for the free-fall time of the atomic gas (see Equation 14) yields an efficiency $\epsilon_{\text{ff}}$ of 1 per cent, which is also the SFE of the molecular gas. In other words the atomic gas is consumed at the same rate as molecular suggesting their ratios are fixed.

Dwarf galaxies are $\text{HI}$ dominated and so the molecular fraction is expected to be low, which also simultaneously leads to a lower effective SFE of the total gas. Measuring the molecular fraction in low-metallicity galaxies is challenging, due to the very high ratio of CO-to-$\text{H}_2$ column densities (Bolatto, Wolfire & Leroy 2013), although CO observations (e.g. Schruba et al. 2012) and dust emission studies (Bolatto et al. 2011) suggest that the molecular gas fraction should be very low. For example, Bolatto et al. (2011) derive a molecular fraction of only 5 per cent for the Small Magellanic Cloud (SMC) using high-resolution $\text{HI}$ and dust emission maps. Given that the SFE of the atomic gas and molecular gas are found to be similar, it should be possible to estimate the fraction of molecular gas by comparing the atomic and molecular star formation laws and having adjusted for free-fall times (or in our case a disc thickness factor).

Although evidence in general supports dwarf irregulars having thick discs (e.g. Roychowdhury et al. 2010; Elmegreen & Hunter 2015), direct measurement of the three-dimensional shape of the dwarf galaxies DDO 46 and DDO 168 using the central stellar dispersion to the ratio of the maximum rotation speed by Johnson et al. (2015) suggests that these galaxies are comprised of thin stellar disc. If gas discs in dwarf galaxies were also thin, the estimation of the molecular fraction in these systems should also account for the possibility of varying disc thickness and free-fall times.

To attempt an estimation of the typical molecular fraction we consider only variations in disc scaleheight and molecular fractions. We ignore other factors that might affect the SFE. First, we assume that disc scaleheights are largely consistent within the dwarf galaxy sample and following Roychowdhury et al. (2010) the disc thickness is statistically $\sim 2.5$ times thicker than the typical spiral. Using the relationship between molecular gas and SFR surface densities from Leroy et al. (2013b), our galaxies are offset by a factor of approximately 15–20 to the expected value. However since the disc is potentially 2.5 times effectively less dense than for those in spirals due to an increased scaleheight, this factor is perhaps closer to six to eight times corresponding to a typical molecular fraction of $\sim 0.16$, or in the case of a thin disc to 0.05.

In their analysis of a sample of LSB galaxies, Wyder et al. (2009) suggested that a relative decrease in the molecular fraction in environments below the saturation limit, $\Sigma_{\text{sat}} \approx 9 \text{M}_\odot \text{pc}^{-2}$ is a possible explanation for the decreased SFE. Following the suggestions of Blitz & Rosolowsky (2006) that the ratio of molecular-to-atomic gas in galaxies is determined by hydrostatic pressure in the ISM, which is a function of the stellar surface density, the gas surface density, and the gas-to-stellar velocity dispersion ratio, Wyder et al. (2009) argue that the LSB galaxies will invariably have a lower ISM pressure and thus lower molecular fraction.

We explore this possibility by examining the $H$-band mean effective surface brightness against the SFE for the KRDJ08 and YJK14 samples in Fig. 7. As discussed in KRDJ08 and YJK14, we can use the $H$-band surface brightness as a proxy for stellar surface density, $\Sigma_{\text{star}}$. The data in Fig. 7 cover six orders of magnitude in...
surface brightness and are well scattered with a minor trend towards higher SFE with higher surface brightness. A linear fit to the data (red continuous line in Fig. 7) provides a correlation coefficient of \( r = -0.645 \). This suggests that the stellar densities play a minor role in setting the SFE amongst the various dwarf galaxies. Many of the galaxies in Fig. 7 approach surface brightnesses typical of late-type spirals found in the 2MASS Large Galaxy Atlas (Jarrett et al. 2003) yet have a much larger range of SFEs. In relative terms, it would appear that the lower stellar densities relative to the spiral population play a minor role in setting the SFE.

However, we note that, following Shi et al. (2011) and Wang et al. (2017), an effect of the \( \Sigma_{\text{gal}} \) should be expected, as introduced in the extended Schmidt law. Recently Roychowdhury, Chengalur & Shi (2017) used data from the FIGGS survey to show that low-metallicity dwarf galaxies also followed the extended Schmidt law. They found that the mean deviation of the FIGGS galaxies from the extended Schmidt law is 0.01 dex, with a scatter around the relation of less than half of that seen in the original Shi et al. (2011) relation. A precise determination of the SFE (i.e. performing a detailed SFR study and deriving the amount of neutral gas using interferometric maps) should be obtained to explore further this issue using our galaxy sample.

### 4 COMPARISONS TO MODELS

In the previous sections, we attempted to describe the vertical offset displayed by the dwarf galaxies in Fig. 6 in terms of variations in their disc or molecular fraction. Krumholz, Dekel & McKee (2012) demonstrated that in the case of the molecular star formation relation, much of the observed scatter could be reduced by normalizing the molecular gas mass per free-fall time,

\[
\Sigma_{\text{SFR}} = f_{\text{H}_2} \epsilon_t \frac{\Sigma_{\text{gas}}}{\sqrt{G}} \quad (14)
\]

\[
t_{\text{ff}} = \sqrt{\frac{\pi}{32 \epsilon_t \rho}} \quad (15)
\]

where \( \rho \) is the density of the star-forming complex, \( f_{\text{H}_2} \) is the fraction of the molecular gas, and \( \epsilon_t \) is a dimensionless SFE scalefactor. Since in extragalactic observations of regular spirals the resolution does not approach that of a giant molecular cloud, the mean surface gas densities are instead representative of the ISM. In the case where star formation occurs in a galaxy primarily through GMC complexes, Krumholz et al. (2012) show that the free-fall time can be estimated from easily observed projected quantities,

\[
t_{\text{ff}} = \frac{\pi^{1/4}}{\sqrt{G}} \frac{\sigma}{\left( \Sigma_{\text{GMC}} \Sigma_{\text{gal}} \right)^{1/4}} \quad (16)
\]

where \( \Sigma_{\text{GMC}} \) is the mean gas surface density of GMC values adopted from local observations, \( \sigma \) is the local velocity dispersion of the gas, and \( \Sigma_{\text{gal}} \) is the average gas surface density in the region of the galaxy where the GMCs form. Since variations in disc scaleheight should result in relative changes of the volume density of the gas and therefore the free-fall time, for a given mean value of the gas velocity dispersion within the star-forming disc, the free-fall time could be estimated. Applying Equation 14, having now accounted for projection effects, any remaining vertical offset between dwarf and spiral galaxies could be more precisely attributed to variations in \( f_{\text{H}_2} \), the molecular fraction of the gas.

As demonstrated by Leroy et al. (2013b) and Shetty et al. (2014), any star formation relation is ultimately a multidimensional problem and potentially even a multivalued function of \( \Sigma_{\text{gas}} \). Using observations to constrain the inputs, comparisons to models with varying underlying theoretical assumptions could provide greater insight into the processes that regulate star formation. Indeed, the correlation between atomic gas and the SFR surface densities in H-dominated regimes, as demonstrated in this study and others (Bigiel et al. 2010; Bolatto et al. 2011; Roychowdhury et al. 2014, 2015), has been the subject of interest in recent models (Ostriker et al. 2010; Krumholz 2013) whose underlying theoretical assumptions differ.

In the Ostriker et al. (2010) model (hereafter OML), the ISM comprised warm and cold diffuse gas and a gravitationally bound phase. Star formation occurs in the gravitationally bound component without explicit treatment of its chemical state, at a rate corresponding to a fiducial choice in gas depletion timescale of 2 Gyr. The ISM satisfies thermal and vertical hydrostatic equilibrium whereby the UV heating (proportional to the SFR) can be balanced against the midplane density. The transition from H - to H$_2$-dominated gas, and the effect gas metallicity has on it in the OML10 model, is not treated explicitly but manifests itself instead where the composition of the ISM transitions from mostly diffuse to mostly gravitationally bound. This transition happens smoothly, and will be an important factor when comparing models later. Alternatively, the Krumholz (2013, hereafter, KMT+) model, a low surface density extension to Krumholz et al. (2012, hereafter KMT), explicitly determines the fraction of gas in the molecular phase that corresponds to the gas phase that is eligible to form stars. The fraction of the gas that is H$_2$ is calculated from the gas metallicity through dust shielding and through the photo-dissociation rate, as described in Krumholz, McKee & Tumlinson (2008, 2009). Perhaps motivated by a desire to reproduce recent resolved observations of H$_2$-dominated galaxies (Bigiel et al. 2010) and the SMC (Bolatto et al. 2011), Krumholz (2013) successfully developed a model that predicts a floor in the SFR surface density. They argue that the interstellar radiation field intensity is not sufficient enough to satisfy hydrostatic equilibrium in the ISM of H$_2$-dominated galaxies. By considering hydrostatic balance alone, a ‘floor’ value on the density of the cold atomic phase can be determined, which can then be equated to a molecular fraction and SFR.

Fig. 8 compares the KMT+, OML, and the Bolatto et al. (2011, hereafter, OML+) (modification of the original OML by introducing an extra metallicity dependence). These models have been computed with the following parameters. Based on the discussions of Ostriker et al. (2010) and Krumholz (2013) we adopted a ratio of the mass-weighted mean thermal velocity dispersion, where if significant warm neutral medium is present, it is approximately equal to the fraction of diffuse warm gas, \( f_{\text{w}} \approx f_{\text{w}} = 0.5 \). Variations in this quantity are degenerate with the midplane density parameter, \( \rho_{\text{mid}} \), for which we have adopted values in the range of 0.3–0.003 \( M_{\odot} \) pc$^{-2}$ in line with the ranges in other studies (Krumholz 2013; Roychowdhury et al. 2015, 2014). For the OML and OML+ models, values of the observed total velocity dispersion divided by the mean thermal value are ranged from 2 to 10 as per their discussions to produce the widest range in model tracks. For the KMT+ model, a clumping factor of \( f_{\text{c}} = 5 \) is adopted, which is the expected reduction factor in the mean surface density of cloud complexes when averaged over the ISM on kpc scales. All models are computed with a stellar metallicity of \( Z = 0.1 Z_{\odot} \).

Fig. 8 illustrates the success with which these models describe various data sets. The H$_2$-dominated outer disc data from Bigiel et al. (2010) is well described by the OML+ and KMT+ models. However, Roychowdhury et al. (2015) observations matched better with the predictions of the OML model than those provided by the KMT model for galaxies of all types. The physical implications
The log SFR versus total gas surface densities. Dwarf galaxies are assumed to have a negligible molecular fraction and so their total gas surface density is simply the atomic gas corrected for the presence of helium using a factor of 1.34. The K98 galaxies have been corrected for the presence of helium contrary to the original work. Filled triangles indicate disc-averaged quantities for the galaxies whose column densities were measured directly from Roychowdhury et al. (2014) and Wyder et al. (2009) studies. Open circles indicate galaxies whose total gas surface densities have been estimated using global HI properties as described in the text. The grey-scale-smoothed distribution represents the outer disc data of HI-dominated dwarf and spirals from Bigiel et al. (2010) (shown in Fig. 6 as stars with errorbars). The models are indicated by the lines in the legend and are described in detail in the text.

The implication is that in the outer discs of spirals and dwarf galaxies, hydrostatic balance alone is sufficient to describe the SFRs, but mean values of the overall discs of these low-mass galaxies suggest that thermal pressure provides an important contribution and is required to explain the full range of the data. This is consistent with the conclusions of Elmegreen & Hunter (2015) who found that models considering thresholds in the presence of H2 did not agree with the smooth trends observed for the discs of the dIrr sample.

It is worth noting that two orders of magnitude in midplane density is quite generous, and although in general we do not have a handle on this quantity, $0.3 M_\odot pc^{-2}$ is already a factor of 10 times larger than values that have been inferred in galaxies (Bruzzone et al. 2015). Restricting this value further suggests that the OML model underpredicts the observed SFR densities. Alternatively, the original KMT model (Krumholz et al. 2009b) can describe the full range of the data if one relaxes the restriction on the clumping factor, $f_c$. Fig. 9 compares the KMT and KMT+ models with a range of $-0.3 < \log_{10}(f_c Z_\ast) < 1.2$, and in the case of the KMT+ model, a range of midplane densities an order of magnitude smaller than in Fig. 8 ($0.03–0.003 M_\odot pc^{-3}$) was adopted. The original KMT model adequately describes the full range of the data with these model parameters. However while perhaps appropriate when describing variation in spiral galaxies, a $\log_{10}(f_c Z_\ast)$ value of 1.2 for a metallicity $Z_\ast = 0.1 \odot$ in units of solar metallicity suggests clumping factors an order of magnitude higher than that fiducial value of five adopted here and in tension with observations (Leroy et al. 2013a).

Variations in the underlying IMF and non-constant star formation history (SFHs) leading to systematic variations in the SFR estimates may explain this discrepancy. Although a full treatment of this topic is outside the scope of this work, we redirect the reader to Fumagalli et al. (2011), Weisz et al. (2012), and Boquien, Buat & Perret (2014). Recent observations with the STARBIRDS sample of galaxies by...
McQuinn et al. (2015) suggest an empirical calibration of the FUV-based SFR relation for dwarf galaxies, which is ~53 per cent more than Hao et al. (2011) which would increase the SFRs by a factor of 1.5 and further worsens agreement between the models and data presented here.

5 SUMMARY

We have provided a method for estimating the surface density of the atomic gas from global HI parameters that are widely available from HI surveys, and precision geometric parameters available from stellar photometry. We test this method using two control samples and find the approximation overestimates the actual surface gas density in HI-dominated galaxies to within a factor of 0.5 dex. We apply this method to a sample of 147 galaxies drawn from modern NIR stellar photometric surveys cross-correlated with available FUV and 24 µm fluxes to estimate the SFR surface density.

With this sample we confirm a strict correlation between the HI surface gas density and the SFR surface density with a sample of dwarf galaxies an order of magnitude larger than previous works. We find that the SFE of HI-dominated gas is offset from that in HI surveys, and precision geometric parameters available from stellar photometry. We test this method using two control samples and find the approximation overestimates the actual surface gas density in HI-dominated galaxies to within a factor of 0.5 dex. We apply this method to a sample of 147 galaxies drawn from modern NIR stellar photometric surveys cross-correlated with available FUV and 24 µm fluxes to estimate the SFR surface density.

We have provided a method for estimating the surface density of the atomic gas from global HI parameters that are widely available from HI surveys, and precision geometric parameters available from stellar photometry. We test this method using two control samples and find the approximation overestimates the actual surface gas density in HI-dominated galaxies to within a factor of 0.5 dex. We apply this method to a sample of 147 galaxies drawn from modern NIR stellar photometric surveys cross-correlated with available FUV and 24 µm fluxes to estimate the SFR surface density.

Finally we have compared our data and others from the literature to available models. We show that no single model can describe the full extent of the data. However these models together suggest that feedback is of variable importance depending on the density regime or galaxy environment, and that the transition from HI- to H2-dominated is a metallicity-dependent process. Mean values of $\Sigma_{\text{SFR}}$, $\Sigma_{\text{gas}}$, and $\Sigma_{\text{star}}$ suggest that globally in these HI-dominated galaxies, thermal pressure is an important regulatory process.

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