Resonant enhancement of the ultracold photoassociation rate by an electric field-induced anisotropic interaction

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Abstract

We study the effects of a static electric field on the photoassociation of a heteronuclear atom pair into a polar molecule. The interaction of permanent dipole moment with a static electric field largely affects the ground state continuum wavefunction of the atom pair at short separations where photoassociation transitions occur according to the Franck–Condon principle. Electric field-induced anisotropic interaction between two heteronuclear ground state atoms leads to scattering resonances at some specific electric fields. Near such resonances the amplitude of the scattering wavefunction at short separation increases by several orders of magnitude. As a result, the photoassociation rate is enhanced by several orders of magnitude near the resonances. We discuss in detail electric field-modified atom–atom scattering properties and resonances. We calculate the photoassociation rate that shows giant enhancement due to electric field tunable anisotropic resonances. We present selected results among which particularly important are the excitations of higher rotational levels in ultracold photoassociation due to electric field tunable resonances.

1. Introduction

Research interest in the field of cold molecules has witnessed a tremendous growth in recent times. The possibility of investigating molecular behaviour at low temperatures motivates physicists and chemists from diverse backgrounds to study cold and dense molecular gases. Certainly, this development is inspired by the great success in the closely related field of cold atoms. Molecules can have properties which are not available with atoms, for instance a heteronuclear molecule can possess permanent electric dipole moment. While the rich internal structure of molecules possesses new challenges for cooling and trapping them, the potential applications of cold molecules are remarkable. This is especially true for ultracold polar molecules which allow for a wealth of interesting studies. The interaction of permanent dipoles with an external electric field provides a tool to manipulate physical processes taking place in the ultracold regime. Several quantum computation devices have been proposed based on the interaction of the heteronuclear dimers with external electric fields [1, 2]. External electric fields can also alter the internal rovibrational structure and dynamics of heteronuclear molecules [3–5]. The orientation, angular motion, hybridization and changes in the transition rates and lifetimes of the rovibrationally excited state of a LiCs molecule in a strong static electric field have been theoretically studied [6, 7]. Electric field is used to enhance the interaction between Li and Cs atoms in an ultracold collision [8, 9]. This enhancement is due to the interaction of the instantaneous dipole moment of the heteronuclear collision complex with the static electric field. The interaction of a heteronuclear pair of atoms with an electric field can couple states of different angular momenta in the electronic ground continuum of the pair leading to resonances in an ultracold collision.

Our purpose here is to utilize the static Electric field-induced scattering resonances to influence the free-bound photoassociation (PA) [10] process of molecule formation. PA of ultracold atoms via the interaction with an electromagnetic
field has become a standard technique to produce cold and ultracold molecules. The experimental techniques previously used for the formation of homonuclear molecules have been extended to heteronuclear alkali–metal dimers. Several experimental groups have reported the photoassociative formation of ultracold alkali–metal dimers, such as NaCs [11], KRB [12–14], RbCs [15, 16] and LiCs [17] in their electronic ground states. The effect of a static electric field on the formation of heteronuclear molecules in their electronic ground state via one-photon stimulated emmision from ground continuum has been theoretically studied [18].

Here, we investigate the effect of a static electric field on the PA process of a heteronuclear atom pair to produce molecules in an excited electronic state. Since an electric field can couple different angular momentum states (partial waves), we need to investigate anisotropic scattering at low energy. Taking the LiCs molecule as a prototype, we first present a detailed investigation of low-energy anisotropic atomic collision in the presence of a static electric field. We have used Numerov–Cooley algorithm-based multichannel scattering techniques and found several anisotropic resonant structures in the scattering cross-sections of the $^7\text{Li} + ^{133}\text{Cs}$ collision. Although the effects of a magnetic Feshbach resonance [19] on PA have been recently studied both experimentally [20, 21] and theoretically [22–26], to the best of our knowledge, the effects of electric field-induced anisotropic resonances on PA into excited molecular levels have not yet been studied. One notable feature of the influence of these anisotropic resonances on PA is the occurrence of higher rotational excitations in the excited molecule. This follows from the large modification of two-atom continuum wavefunctions for higher partial waves. Owing to the strong spatial dependence of permanent dipole moment at short separations, the interaction of a static electric field with the permanent dipole moment of a heteronuclear atom pair leads to large enhancement of continuum wavefunctions at short separations, near electric fields at which anisotropic resonances occur.

This paper is organized as follows. First, we briefly discuss how an external static electric field modifies the effective interaction potential between two heteronuclear collision pairs. In section 2, we present mathematical formulation of the problem with an emphasis on anisotropic scattering. The effects of an external static electric field on the ground state scattering of $^7\text{Li} + ^{133}\text{Cs}$ are discussed in section 3. In section 4, we discuss the effects of a static electric field-induced anisotropic interaction on the PA rate and present our main results. Finally, we summarize and come to the conclusion in section 5.

2. Formulation

The dynamics of the Li–Cs collision in the presence of an electric field is effectively described by the radial Hamiltonian

$$\hat{H}_R = -\frac{1}{2\mu R} \frac{\partial^2}{\partial R^2} + \frac{\hat{L}^2(\theta, \phi)}{2\mu R^2} + \hat{V}_E(R) + \hat{V}_{hf} + \hat{V}_c$$  \hspace{1cm} (1)

Figure 1. Adiabatic Born–Oppenheimer potentials of LiCs without hyperfine interaction for excited (a) and ground (b) states. The ground state asymptotically corresponds to both Li and Cs atoms in the electronic S state while the excited state corresponds to Li in the S state and Cs in the P state.

where $\mu = m_1m_2/(m_1 + m_2)$ is the reduced mass of two atoms $^7\text{Li}$ and $^{133}\text{Cs}$ with masses $m_1$ and $m_2$, respectively, $R$ is the interatomic distance, $\hat{L}^2$ is the rotational angular momentum of the collision complex and the angles $\theta$ and $\phi$ specify the orientation of the interatomic axis in the space-fixed coordinate frame. The electronic interaction potential can be represented as

$$\hat{V}_E(R) = \sum_S \sum_{M_S} \langle SM_S | V_S(R) | SM_S \rangle$$  \hspace{1cm} (2)

where $S$ is the total electronic spin of the two atoms and $M_S$ is the projection of $S$ on the Z-axis. $V_S(R)$ represents the adiabatic interaction potential of the molecule in the spin state $S$. The ground state $V_g(R)$ and the excited state $V_e(R)$ potentials, as shown in figure 1, are taken from [27] and [28], respectively. This interaction is therefore diagonal in the adiabatic basis $|1M_1; SM_S\rangle$:

$$\langle S'M'_{S'}; I'M'_I | \hat{V}_E(R) | SM_S; I'M_I \rangle = \delta_{S'S} \delta_{I'I} \delta_{M'S} \delta_{M'M} \langle V_S(R) \rangle$$  \hspace{1cm} (3)

where $S = S_1 + S_2$ and $I = I_1 + I_2$, $S_1$ and $S_2$ are the electronic spins, while $I_1$ and $I_2$ are the nuclear spins of the Li and Cs atoms, respectively. The total hyperfine Hamiltonian $\hat{V}_{hf}$ for the collision complex can be written as a sum of the two atomic hyperfine Hamiltonian

$$\hat{V}_{hf} = \sum_{j=1}^{2} \frac{\hat{a}_h(j)}{R^2} \hat{s}_j \cdot \hat{i}_j = \sum_{j=1}^{2} \frac{\hat{a}_h(j)}{2\hbar} (\hat{j}_j^2 - \hat{s}_j^2 - \hat{i}_j^2)$$  \hspace{1cm} (4)

where $\hat{f}_j = \hat{s}_j + \hat{i}_j$ is the total spin and $\hat{a}_h(j)$ is the hyperfine constant of the atom $j$, which is 402.00 MHz for $^7\text{Li}$ and 2298.25 MHz for $^{133}\text{Cs}$ [29]. This hyperfine interaction is diagonal in the atomic or diabatic or long-range basis $|\ell, f, f_1, f_2\rangle$ in which $\hat{V}_c(R)$ can be expressed as

$$\langle (f_1 f_2) f' m_f \ell' m_{\ell} | \hat{V}_c(R) | (f_1 f_2) f m_f \ell m_{\ell} \rangle = \sum_{S'M; I'M; \ell' \ell} V_{S'}(SM_S; I'M_I; \ell' \ell \ell) \langle (f_1 f_2) f' m_f \ell' m_{\ell} | S'M'_S; I'M'_I; \ell' \ell' \ell \rangle.$$  \hspace{1cm} (5)
where \( \langle \) part of the potentials.

The transformation from coupled hyperfine representation to short-range representation is given by

\[
\langle \text{SM}_S | IM_I | f m_f \rangle \langle f m_f | \ell m_c \rangle = \delta_{\ell \ell'} \delta_{m m_c} \langle \text{SM}_S | IM_I | f m_f \rangle
\]

\[
\times \sqrt{(2 f_1 + 1)(2 f_2 + 1)(2 S + 1)(2 I + 1)} \begin{pmatrix} s_1 & i_1 & f_1 \\ s_2 & i_2 & f_2 \\ S & I & f \end{pmatrix}
\]

where \( \langle \text{SM}_S | IM_I | f m_f \rangle \) is the Clebsch–Gordon coefficient and the quantity in curly bracket is 9-j-symbol. The hyperfine Hamiltonian can only couple channels with the same total angular momentum projection \( m_f = m_f + m_{f_2} = M_S + M_I \) where \( m_f, m_{f_2}, M_S \) and \( M_I \) are the projections of \( f_1, f_2, S \) and \( I \) respectively. For \(^7\)Li, \( f_1 = 3/2 \), and for \(^{133}\)Cs, \( f_2 = 7/2 \) (both with \( s_1 = s_2 = 1/2 \)). Since \( m_f \) takes values from \(-6\) to \(+6\), the total degeneracy of the atom pair is 128. However, atoms mainly collide on the Li(\(^2\)S\(_1/2\), \( f_1 = 2 \)) + Cs(\(^6\)S\(_1/2\), \( f_2 = 3 \)) channel, and thus only 35 degenerate entrance channels have to be considered. For \( f = 5 \), three collisional channels are possible, as given in table 1. The potentials of these three channels are shown in figure 2. We consider a single asymptotic hyperfine channel (c) with \( f_1 = 2, f_2 = 3 \) since the difference in energy of this channel from the other two channels is large enough compared to collision energy at ultracold temperatures. Thus, we can approximate our calculation as a single channel with \( f_1 = 2, f_2 = 3 \). The operator \( \hat{V}_E (R) \) describes the interaction of the atoms with an external electric field. It can be written in the form

\[
\hat{V}_E (R) = -E \cos \theta \sum_S \sum_M \langle \text{SM}_S | d_S (R) | \text{SM}_S \rangle
\]

where \( d_S (R) \) denotes the dipole moment functions of LiCs in the different spin states and \( E \) the electric field magnitude. Li and Krems [9] have given an analytical expression for this dipole moment function approximating the numerical data computed by Aymar and Dulieu [30]. This analytical expression is given by

\[
d_S (R) = D \exp[-\alpha (R - R_e)^2],
\]

with the parameters \( R_e = 0.5 \text{ Debye} \) for the singlet state and \( D = 0.5 \text{ Debye} \) for the triplet state (where \( a_0 = \text{Bohr radius} \)). The matrix element of \( \hat{V}_E (R) \) is evaluated using the expressions

\[
\langle \ell m_c | \cos \theta | \ell' m_c' \rangle = \delta m_c m_c' \left( \begin{array}{cc} \ell & 1 \\ -m_c & 0 \end{array} \right)
\]

\[
\times \left( \begin{array}{cc} 1 & \ell' \\ 0 & 0 \end{array} \right) \left[ (2\ell + 1)(2\ell' + 1) \right]^{1/2}
\]

and

\[
\langle \text{SM}_S | \sum_{S'} \sum_{M_{S'}} | S'M_{S'} \rangle d_{S'} \langle S'M_{S'} | \text{SM}_S \rangle = d_S \delta_{SS'} \delta_{M_S M_{S'}}
\]

where \( (\vec{R} | \ell, m_c) \) is the \( Y_{\ell m_c} \). Due to the symmetry of the z-component of the angular momentum, the matrix element \( \langle \ell m_c | \cos \theta | \ell' m_c' \rangle \) exists only if \( \ell - \ell' = \pm 1 \) and \( m_c = m_c' \). Therefore, the electric field can couple even and odd parity channels to each other but not to themselves.

The scattering wavefunction can be expressed as

\[
\Psi(\vec{R}) = \frac{1}{\vec{R}} \sum_{\ell m_c} \psi_{\ell m_c}(R) Y_{\ell m_c}^{*}(\vec{k}) Y_{\ell m_c}(\vec{R})
\]

which has the asymptotic form

\[
R \Psi(\vec{R}) \sim R \exp(i \vec{k} \cdot \vec{R}) + f_{\vec{k} \vec{k'}} \exp(i \vec{k} \cdot \vec{R}),
\]

where \( \vec{k} \) and \( \vec{k'} \) are the incident and the scattered momentum, respectively. The on-shell elastic scattering is then described by \( f_{\vec{k} \vec{k'}} \), with the scattered momentum \( \vec{k} = k \vec{R} \). Expanding the scattering amplitude \( f_{\vec{k} \vec{k'}} \) into the complete basis \( Y_{\ell m_c} \), we have

\[
f_{\vec{k} \vec{k'}} = \frac{4\pi}{k} \sum_{\ell m_c} T_{\ell m_c}(\vec{k}) Y_{\ell m_c}(\vec{R})
\]

where \( T_{\ell m_c} \) is a \( T \)-matrix element which can also be expanded in the following form:

\[
\frac{1}{k} T_{\ell m_c}(\vec{k}) = \sum_{\ell' m_c} i^{\ell} j_{\ell}(kR) Y_{\ell m_c}^{*}(\vec{k}) Y_{\ell m_c}(\vec{R}),
\]

and

\[
\exp(i \vec{k} \cdot \vec{R}) = 4\pi \sum_{\ell m_c} i^{\ell} j_{\ell}(kR) Y_{\ell m_c}^{*}(\vec{k}) Y_{\ell m_c}(\vec{R}).
\]
Substituting equations (13) and (15) into equation (12) we obtain
\[
R \Psi(\vec{R}) \sim \frac{4\pi}{k} \sum_{\ell_m} i^\ell |V_{\ell_m}(\vec{k})| \sin(kR - \ell \pi/2) + T_{\ell_m}(\vec{k}) \times \exp(i k R - i \ell \pi/2) |Y_{\ell_m}(\vec{R})|
\]
(16)
where the asymptotic form \(j_{\ell}(kR) \sim \sin(kR - \ell \pi/2)/(kR)\) has been used. We obtain the multichannel form of the scattering equation which is given by
\[
h_\ell \psi_{\ell m}(R) = \sum_{\ell', m'} |\ell'| l |V_{\ell'}(R) \langle \ell' m' | \psi_{\ell m}| \psi_{\ell m'}|,
\]
(17)
where
\[
h_\ell = -\frac{\hbar^2}{2\mu} \frac{d^2}{dR^2} + \frac{\hbar^2}{2\mu} \frac{\ell(\ell + 1)}{R^2} + V - E.
\]
(18)
\(E = \hbar^2 k^2/2\mu\) is the collision energy and \(V\) is the central potential for the chosen hyperfine channel. The asymptotic boundary condition on \(\psi_{\ell m}\) can be set as
\[
\psi_{\ell m} \sim j_{\ell}(kR - \ell \pi/2) + T_{\ell m}(k) \exp(i k R - i \ell \pi/2).
\]
(19)

Under the approximation of a single asymptotic hyperfine channel as discussed earlier, we can write the coupled equation (17) in a matrix form in a relative angular momentum (\(\ell\)) basis as given by
\[
[\left[\left(-\frac{\hbar^2}{2\mu} \frac{d^2}{dR^2} + V\right) I + \frac{\hbar^2}{2\mu} \frac{\ell(\ell + 1)}{R^2} \right] + V_R] \Phi = E \Phi
\]
(20)
where \(I\) is the identity matrix, and \(L^2 \equiv \text{Diag}[1(1 + 1), 2(2 + 1), \ldots, \ell(\ell + 1), \ldots]\) is a diagonal matrix. The wavefunction \(\Phi\) is a matrix whose elements are given by \(\phi_{\gamma'}\), where \(\gamma \equiv \ell, m_\ell\) and \(\gamma' \equiv \ell', m_{\ell'}\) are the incident and the scattered angular states respectively. Therefore, the overall wavefunction for an incident partial wave \(\gamma(\ell, m_\ell)\) becomes
\[
\psi_{\gamma = \ell, m_\ell}(E, R) = \sum_{\gamma' = \ell', m_{\ell'}} \phi_{\gamma'}(E, R) |\gamma'\rangle.
\]
(21)

By imposing the boundary conditions on the partial waves as given by equation (19), we can obtain the \(T\)-matrix elements, \(T_{\ell m}\). The total elastic cross-section is given by
\[
\sigma = 4\pi \sum_{\ell' m' m_{\ell'}} |T_{\ell m}|^2.
\]
(22)

3. Ground state scattering: electric field-induced resonances

To obtain asymptotic scattering solutions, the Numerov technique was adopted to numerically propagate equation (20). In the asymptotic region, the free wavefunction is given by
\[
\phi_{\ell m} = c_1 \sin(kR - l \pi/2) + c_2 \cos(kR - l \pi/2).
\]
(23)

We construct the \(S\)-matrix with its elements given by \((c_1 - ic_2)^{-1}(c_1 + ic_2)\) and the \(T\) matrix \((S - I)/(2i)\). In the absence of electric fields, different partial wave states of the Li–Cs collision complex are uncoupled and s-wave scattering almost entirely determines the cross-sections at ultralow kinetic energies. The interaction of permanent dipole moment of the colliding pair of heteronuclear atoms with the electric field as given by equation (7) induces coupling between different angular momentum states and may thus affect the ground state scattering wavefunctions. Ultracold s-wave scattering is isotropic: the probability to find the atoms after s-wave collisions does not depend on the scattering angle. The interaction with electric fields however couples the spherically symmetric s-waves to anisotropic p-waves which in turn is coupled to d-wave, d-wave to g-wave and so on. Figure 3 shows anisotropic resonance structures in the scattering cross-section of the \(^{7}\text{Li} + ^{133}\text{Cs}\) collision at 50 \(\mu\text{K}\) energy. Typically convergent results are obtained for a minimum angular momentum of \(\ell = 9\), as shown in figure 3. The larger the electric field, the larger the number of partial waves required for convergence. We get the first resonance peak near 1298 \(\text{K}\) \(\text{cm}^{-1}\) and the second one near 1650 \(\text{K}\) \(\text{cm}^{-1}\). To show the effect of these resonances on PA, we have carried out PA calculations near the first resonance peak.

The permanent dipole moment function of the collision complex as given by equation (8) is typically peaked around the equilibrium distance of the diatomic molecule in the ground state and quickly decreases as the atoms separate. Due to this strong spatial dependence of permanent dipole moment at short separations, the interaction of a static electric field with the permanent dipole moment of the collision pair leads to large modification of continuum wavefunctions at short separations. Figure 4 demonstrates that the modification is particularly significant near the resonant electric fields. Since PA transitions take place at short separations near the outer turning point of \(B^1\Pi\) modification of the continuum wavefunctions at short separations influences PA transition probability as described in the following section.
and given by $R$ resonant electric field $S$ $K$ $Li(22$ of electric field effects on PA, we consider PA transition from ground state by a two-step PA procedure [31]. For illustration an ultracold bosonic $7Li\,^{133}Cs$ molecule in their rovibrationalRecently, an experiment has demonstrated the formation of $4$. Photoassociation: electric field effects

Recently, an experiment has demonstrated the formation of an ultracold bosonic $^7Li\,^{133}Cs$ molecule in their rovibrational ground state by a two-step PA procedure [31]. For illustration of electric field effects on PA, we consider PA transition from $Li(2^2S_{1/2}, f_1 = 2) + Cs(6^2S_{1/2}, f_2 = 3)$ continuum to the $v = 26, J = 1$ level of $B^1\Pi$, near the electric fields at which anisotropic resonances occur. The PA rate coefficient [32] is given by

$$K_{PA}(T, \omega_L) = \left\langle \frac{\pi v_{rel}}{k^2} \sum_{\ell = 0}^{\infty} (2\ell + 1) |S_{PA}(E, \ell, \omega_L)|^2 \right\rangle$$  \hspace{1cm} (24)

where $v_{rel} = \hbar / \mu$ is the relative velocity of the two atoms, $S_{PA}(E, \ell, \omega_L)$ is the $S$-matrix element for the process of loss of atoms due to PA and $\{\ldots\}$ implies an averaging over thermal velocity distribution. Assuming Maxwell–Boltzman distribution at temperature $T$ we have

$$K_{PA}(T, \omega_L) = \frac{1}{\hbar Q_T} \sum_{\ell = 0}^{\infty} (2\ell + 1)$$

$$\times \int_0^{\infty} |S_{PA}(E, \ell, \omega_L)|^2 e^{-E/k_B T} \ dE$$  \hspace{1cm} (25)

where

$$|S_{PA}(E, \ell, \omega_L)|^2 = \frac{\Gamma \gamma_\ell}{[(\delta + E - \omega_L) / \hbar]^2 + (\Gamma / \gamma_\ell)^2].$$  \hspace{1cm} (26)

Here $Q_T = (2\pi \mu k_B T / \hbar^2)^{3/2}$ is the translational partition function and $\gamma_\ell$ is the natural linewidth of the photoassociated level. $E = \mu v_{rel}^2 / 2$ is the relative kinetic energy of the colliding pair of atoms with reduced mass $\mu$, $E_{v,J}$ is the bound state energy and $\delta = \omega_L - \omega_A$ is the frequency offset between the laser frequency $\omega_L$ and the atomic resonance frequency $\omega_A$. The stimulated linewidth $\Gamma$ is given by

$$\Gamma = \frac{\pi I}{\epsilon_0 c} |\langle \phi_{v,J} | D_\ell (R) | \psi_{\gamma, m_\gamma} (E, R) \rangle|^2$$  \hspace{1cm} (27)

where $I$ is the intensity of the PA laser, $\epsilon_0$ and $c$ are the vacuum permittivity and speed of light, respectively. $D_\ell (R)$ is the transition dipole moment. At zero electric field and for $50\, \mu K$ collisional energy we find $\Gamma = 0.315\, kHz$ at laser intensity $1\, W/\text{cm}^2$. Figure 5 demonstrates that the stimulated linewidth as a function of the electric field $E$ has a resonant structure with giant enhancement near the resonant electric field even at low laser intensity. This is because of large modifications of continuum wavefunctions at short separations. To know which components $\phi_{\gamma', \gamma}$ of the continuum wavefunctions have significant contribution to such resonant enhancement of $\Gamma$, we plot a square of the Franck–Condon (FC) overlap integral $| \eta |^2$ for a few wave components $\phi_{\gamma, 0}$ in figure 6. $\eta$ is defined by

$$\eta = \langle \phi_{v,J} | \psi_{\gamma', m_\gamma} (E, R) \rangle = \langle \phi_{v,J} | \sum_{\gamma' = \ell, m_\gamma} \phi_{\gamma', \gamma} (E, R) | \gamma' \rangle.$$

$$\hspace{1cm} (28)$$

In fact, we find that a large number of partial waves significantly contribute to the resonant features. This is perhaps due to the formation of a quasibound complex inside the centrifugal barrier of a large number of partial waves which are strongly coupled among them. Figure 7 shows that $K_{PA}$ near the resonant electric field increases by four orders of magnitude compared to that at the zero electric field. This enhancement is due to the electric field-induced coupling between different partial waves. The coupling is so strong that higher rotational levels of the excited electronic state can be populated, as shown in figure 8. These higher rotational excitations are not possible at ultracold temperatures in the absence of the electric field. The PA rate increases for rotational levels $J = 3, 4, 5$ and $6$ and then starts decreasing for $J > 7$, as shown in figure 8. This can be understood from figure 9 which shows that the amplitude of $\phi_{v=4, \ell}=0$, $\phi_{v'=5, \ell=0}$
plotted as a function of the atom–field detuning $\delta$
scattered partial waves $E$
incident partial wave $L$
the excited molecular level is larger than $\phi\ell$
transition $|$
with $J$
at a resonant electric field $E$
$\phi\ell$
$\phi\ell$
Figure 7. The photoassociation rate $K_{PA}$ (in unit of $10^{-17}$ m$^3$ s$^{-1}$) is plotted as a function of the atom–field detuning $\delta$ in GHz at the resonant electric field $E = 1298$ kV cm$^{-1}$. The rate increases for $J = 3, 4, 5$ and 6 rotational levels and then starts decreasing for $J > 7$.

and $\phi\ell, l = 0$- wavefunctions near the outer turning point of the excited molecular level is larger than $\phi\ell, l = 0$, $\phi\ell, l = 0$ and $\phi\ell, l = 0$ waves. The selection rule for the free-bound transition $| J - |l + S|| \leq \ell' \leq | J + |l + S||$ allows the scattered partial waves $\ell' = 0, 1$ and 2 to be accessible for PA with $J = 1$. Similarly, higher rotational levels $J > 1$ become populated due to excitations of higher partial waves in the ground continuum through electric field-induced anisotropic scattering.

Enhancement of the PA rate near resonant electric fields critically depends on the outer turning point of the molecular bound state that is accessible to the PA transition. As mentioned earlier, the anisotropic resonances bring about large modification of the amplitude of continuum wavefunctions at relatively short separations. Now, if a prominent antinode of the modified continuum wavefunctions lies at a separation near the outer turning point of the bound state, then enhancement of the PA rate is expected due to large FC overlap. We have chosen a particular bound state for which enhancement can be achieved. Although in this paper we have studied enhancement of the formation rate of excited molecular states only, a similar method of electric field-induced resonances can readily be extended to enhance the formation rate of ground molecular states via one photon stimulated emission [18]. Enhancement can also be achieved using quantum interference [22, 23, 33] via laser coupling another bound state with the continuum. In the case of PA in the presence of a magnetic Feshbach resonance, a quasi-bound state embedded in the ground continuum gives rise to Fano-type quantum interference [23] leading to enhancement in PA [20]. In the case of heteronuclear atoms, quantum interference can be used to enhance the production of ground molecules due to the existence of permanent dipole moment. Recently, an all optical method of quantum interference scheme has been proposed for efficient production of ground state polar molecules [33]. The unique feature of the electric field-induced enhancement would
be the controllability of the excitations of higher rotational states.

5. Conclusion

In conclusion, we have analysed the effects of a static electric field on the PA of a heteronuclear atom pair. Our results show that it is possible to enhance the PA rate by several orders of magnitude by tuning electric field near anisotropic resonances. Due to the anisotropic nature of the interaction, a large number of partial waves in the ground continuum become strongly coupled. As a consequence, higher rotational levels can be populated in an excited dimer formed by PA at ultralow temperatures. This leads to the possibility of selectively populating higher rotational levels in the ground state polar molecule by Raman-type two-color coherent PA. Furthermore, it may be interesting to investigate the effects of the electric field on stimulated Raman adiabatic passage (STIRAP) from free atoms to ground state molecules. Electric field-induced resonances may be coupled with multiple transition pathways to devise novel opto-electrical quantum interference schemes for efficient production of selective rovibrational molecular states.

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