INVESTIGATION OF THE FLOW STRUCTURE IN THE TUNDISH WITH THE USE OF RANS AND LES METHODS

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The liquid steel flow structure in the tundish has a very substantial effect on the quality of the final product and on efficient casting conditions. Numerous model studies are being carried out to explain the effect of the tundish working conditions on casting processes.

It is necessary to analyze the structure of liquid steel flow, which is strongly supported with numerical modeling. In numerical modeling, a choice of a proper turbulence model is crucial as it has a great impact on the flow structure of the fluid in the analyzed test facility. So far most numerical simulations has been done using RANS method (Reynolds-averaged Navier-Stokes equations) but in that case one get information about the averaged values of the turbulent flow. In presented study, numerical simulations using large eddy simulations (LES) method were used and compared to RANS results. In both cases, numerical simulations are carried out with the finite-volume commercial code AnsysFluent.

Keywords: tundish, continuous casting, numerical modeling

1. Introduction

Mathematical models are nowadays the basis for numerical modeling of industrial processes as for example continuous casting of steel. This is due to the fact that investigation of the steel flow field in the continuous casting tundish or removing of non-metallic inclusions in an industrial environment is – due to the high temperatures of the process and the opacity of the liquid steel – difficult, and in some cases even impossible to perform. An adequate and well-developed mathematical model, with appropriate initial and boundary conditions, should be able to reproduce the phenomenon occurring during the steel flow in the real plant [1]. To do so, the results of simulations have to be validated with experimental results, performed on the real plants or at least on its laboratory models. This gives the various opportunities for research to explain the phenomena accompanying the flow of liquid steel in various tundishes during casting process. Most of CFD (Computational Fluid Dynamics) studies in the field of continuous casting were performed with commercial codes, such as Ansys Fluent [2,3] or Phoenics [4,5]. Carried out researches are related to many aspects of the analysis technique of steel casting, including the steel flow and changes of the flow conditions with flow control devices (FCD) [6-8], the residence time distribution [9-11], heat transfer [12,13], and transport and separation of non-metallic inclusions into steel [14-16].

The flow field inside the tundish is strongly investigated with numerical modeling and numerous studies can be found in literature. The turbulence of liquid steel in the tundish is difficult to map accurately [17]. There are areas with a high level of turbulence (shroud and nozzles), and areas with the laminar movement. Since most of numerical researches performed so far are done with RANS method (Reynolds-averaged Navier-Stokes equations), for turbulence modeling, the standard [6,18] or realizable [19,20] k-ε models are mostly used, rather RSM [21,22] (Reynolds Stress Model). In numerical modeling, a choice of a proper turbulence model...
is crucial as it has a great impact on the flow structure of the fluid in the analyzed test facility. In the analysis of the turbulent flow using RANS method one get the averaged values. In case of LES method (Large Eddy Simulation), all the large turbulent scales are solved directly and only the small scales that are smaller than the filter size are modeled. From those simulations one get also the information about the instantaneous velocity field inside the tundish.

2. Investigated tundish

The investigated object is a six-strand continuous casting tundish of a channel-shaped type, equipped with two overflow partitions. The tundish is symmetrical relative to the transverse plane. The nominal capacity of the tundish is 34-tons of liquid steel. It feeds simultaneously six molds for the production of billets with a cross section of 280×300 mm. In its base configuration the tundish is equipped with a pair of dams.

During steady-state casting, with all Submerged Entry Nozzles (SENs) working, the investigated tundish is characterized by a molten steel mass flow of a 138 t/h. The tundish is used for sequence casting with about ten heats. The shape of the tundish together with its basic dimensions are shown in Fig. 1. Table 1 shows the technological operating conditions of the tundish, used also in numerical simulations.

![Fig. 1. Shape (a) and characteristic dimensions (b) of the investigated tundish](image)

| Parameters                  | Value | Units |
|-----------------------------|-------|-------|
| Nominal capacity            | 34    | ton   |
| Molten steel level          | 570   | mm    |
| Shroud diameter             | 86    | mm    |
| SENs diameter               | 36    | mm    |
| Number of tundish nozzles   | 6     | -     |
| Casting speed               | 0.7   | m/min |
| Billets                     | 280x300 | mm |
| Dam height                  | 300   | mm    |
| Dam width                   | 100   | mm    |

The geometry of presented tundish is symmetrical in two planes of symmetry. In the case of calculation performed using RANS method it would be sufficient to calculate only a quarter of the computational domain assuming symmetry boundary conditions at the intersection inside the tundish. Such an assumption could not be used for unsteady simulation using LES method, as this would influence the results – particularly instantaneous solution (this will be shown further in this paper). Due to that authors decided to use full tundish geometry for both methods.

Presented studies are continuation of the previous research performed with tundish water model and RANS calculations [22].

3. Numerical modeling procedures

In LES method (Large Eddy Simulation) a spatial filtering is used to filter out all the scales smaller than the filter size. Using the density-weighted averaging, filtered variables can be written in the form:

\[ \tilde{\phi} = \int_D \phi(x') G(x-x') dx' \] (1)

where D is the computational domain and G is a filter function that determines the size of the resolved scales. The structures that are smaller than the filter size are considered to be unknown and must be modeled. As a result of spatial filtering and Favre averaging procedure applied to continuity and momentum equations, one obtain a system of differential Navier-Stokes equations for LES method:

\[ \frac{\partial \tilde{u}_i}{\partial t} + \frac{\partial}{\partial x_j}(\tilde{u}_i \tilde{u}_j) = -\frac{1}{\rho} \frac{\partial p}{\partial x_i} + \frac{\partial}{\partial x_j}(\mu_{\text{eff}} \frac{\partial \tilde{u}_i}{\partial x_j} + \frac{\partial \tilde{u}_j}{\partial x_i}) \] (3)

with viscosity defined as:

\[ \mu_{\text{eff}} = \mu + \mu_t \] (4)

Using Smagorinsky model [23], subgrid scale turbulent viscosity is described as:

\[ \mu_t = (C_s \Delta)^2 |\tilde{S}| \] (5)

where

\[ \Delta = (\Delta x \Delta y \Delta z)^{1/3} \] (6)

\[ |\tilde{S}| = \sqrt{2S_{ij}S_{ij}} \] (7)

\[ C_s \] is a Smagorinsky model constant (\( C_s \approx 0.1 \)), and the strain rate tensor is defined as:

\[ S_{ij} = \frac{1}{2} \left( \frac{\partial \tilde{u}_i}{\partial x_j} + \frac{\partial \tilde{u}_j}{\partial x_i} \right) \] (8)
To solve the differential equation system, it is necessary to assume suitable initial and boundary conditions, corresponding to the industrial process conditions. To correspond with the real casting conditions in investigated process, the boundary condition for steel flowing through the shroud equals for the velocity of 2.2 m/s and turbulent intensity of 5%. The boundary conditions used in computations are shown in Fig. 2.

In numerical simulation a Standard Wall function has been used (on the bottom and side walls) which based on the work of Launder and Spalding [24]. For both RANS and LES methods the relation between temperature and heat transfer at the wall is defined as:

\[
\frac{(T_w - T_{wall})}{q_w} = \begin{cases} 
\Pr \gamma^* + \frac{1}{2} \Pr \frac{C_{y^*}^{1/2}}{\nu_{eq}} u^* & (\gamma^* < \gamma^*_T) \\
\Pr \left[ \frac{1}{2} \ln(\gamma^*_T) + P \right] + \frac{1}{2} \Pr \frac{C_{y^*}^{1/2}}{\nu_{eq}} \left[ \Pr u_w^2 + (\Pr - Pr_{\text{t}}) u_T^2 \right] & (\gamma^* > \gamma^*_T)
\end{cases}
\]  

(9)

Where \( \gamma^*_T \) is a non-dimensional thermal boundary thickness, defined as a value at which the linear law and the logarithmic law intersect and \( u_c \) is the mean velocity at the distance \( y^* \) from the wall. \( P \) is defined as:

\[
P = 9.24 \left[ \left( \frac{\Pr}{Pr_{\text{t}}} \right)^{1/4} - 1 \right] \left[ 1 + 0.28 e^{-0.007 \Pr_{\text{t}}} \right] \]  

(10)

In case of LES method \( C_\gamma \) values in equation (9) is replaced with the model constant \( C_f \).

Detailed boundary and operating conditions which correspond to the conditions of the industrial process can be found in Table 2. In numerical simulations two cases were studied (Table 3).

### Table 2

| Parameters                     | Value | Units |
|--------------------------------|-------|-------|
| Liquid steel density           | 7010  | kg/m³ |
| Liquid steel dynamic viscosity | 0.007 | kg/m s|
| Inlet velocity                 | 2.0   | m/s   |
| Inlet temperature              | 1823  | K     |
| Specific heat                  | 821   | J/kg K|
| Thermal conductivity           | 30.5  | W/m K |
| Heat flux through side and bottom walls | -2.6  | kW/m² |
| Heat flux through slag cover   | -16   | kW/m² |

Computational grid set at walls of the tundish working space is shown in Fig. 3. The mesh is finer in the shroud and the tundish nozzles regions.

**Table 3**

Parameters and solver settings for analyzed test cases

| Parameters                          | Case A | Case B  |
|-------------------------------------|--------|---------|
| Turbulence method                   | RANS   | LES     |
| Model                               | k-epsilon | Smagorinsky-Lilly |
| Near-wall treatment                 | Standard Wall Function | Standard Wall Function |
| Geometry                            | 3D     | 3D      |
| Mesh type                           | hexa   | hexa    |
| Number of cells                     | 0.9 mln | 2.0 mln |
| Node average distance (whole tundish)| 24 mm  | 15 mm   |
| Node average distance (inlet region)| 6.7 mm  | 6 mm    |
| Time dependency                     | steady | unsteady |
| Time step size [s]                  | -      | 0.01    |
| Pressure velocity coupling          | SIMPLE | SIMPLE  |
| Pressure discretisation             | Standard | Standard |
| Momentum discretisation             | Second Order | Bounded Central Differencing |
| CFD code                            | AnsysFluent 14 [24] | AnsysFluent 14 |

### 4. Results and discussion

The aim of the performed studies was to analyze the flow structure and liquid steel temperature distribution. The results of calculations performed with LES numerical method were compared to RANS results. Numerical model allow to diagnose the working conditions of the investigated tundish. Three-dimensional distributions of steel velocity, as well as the fields of temperature concentrations in the tundish working space, provide a source of good knowledge about steel casting conditions.

In this section, detailed contour maps of the velocity vectors and temperature fields of liquid steel inside the tundish obtained using LES method are presented and compared to RANS results.
Velocity fields and velocity vectors distributions for considered tundish configuration are presented in Fig. 4 and 5. For better analysis of velocity field a maximum and cut-off values were used (left and right columns respectively). The results are presented for the cross section passing through the tundish nozzles. Final results obtained using steady state RANS method were used as an initial condition for LES method. In the case of LES method, mean and instantaneous fields are shown. Mean results correspond to the average values obtained over 3000 seconds of the flow field and the instantaneous value is shown at the final state of the flow field which is \( t = 3000 \) seconds.

Comparing mean velocity field for RANS and LES methods (see Fig. 4a and 4b respectively) one can observe similar velocity distribution close to the inlet area. The differences start to appear in the regions close to the outer SEN’s (number 1, 2, 5 and 6). In this region velocity field obtained using LES method is higher compared to RANS results. LES method provides also information about the instantaneous velocity field, which is presented in Fig. 4c. The differences in the velocity field obtained with RANS and LES methods is also visible in the velocity vectors filed presented in Fig. 5. Higher movements of the liquid steel between SEN’s 1 and 2 and also 5 and 6 is detected by the LES method, whereas for RANS method the velocity in this region is close to 0 m/s. This is also confirmed on the velocity field plotted on the measurement lines presented in Fig. 7. This leads to weaker liquid steel mixing in those regions. This is also confirmed by the temperature distribution inside the tundish working space presented in Fig. 8.
Results obtained with RANS method show higher differences in liquid steel temperatures between inlet zone of the tundish and outer area (close to SEN’s 1 and 6). Due to the better liquid steel mixing predicted by LES method, the temperature field is more uniform in the whole tundish.

Comparing the temperature drop along the investigated tundish for both RANS and LES methods one may observe that this difference is not big – 6 to 12 K – compared to the temperature of incoming liquid steel – 1823 K. In the case of RANS method the temperature drop is bigger and the lowest temperature values are seen in the regions close to the side walls. This can be influenced by the small value of turbulence intensity in those regions and therefore worse mixing. As the LES method is more accurate one may see the temperature distribution drop to be more homogenous along the tundish (see Fig. 9).

Nevertheless, thanks to the flow structure changes caused by the dams, one can observe very low differences between the temperature of incoming steel and the temperature of steel at the ends of the tundish for both RANS and LES methods. With dams, which main task is to control the flow of the liquid steel stream, the movement of warmer fluid in the further tundish areas is possible and liquid steel temperature casted at individual strands is more homogenous. This, in turn, provides stability of the continuous casting process.

5. Summary and conclusions

Investigated tundish is characterized by the thin shape and relatively high ratio of the tundish length to the width, as for common multi-strand tundishes in local steel industry. High velocity of the incoming fluid decreases outside inlet area which is determine by dams. By installation of a pair of dams, two working spaces have been created. The inlet zone is separated from the nozzle zone, which as a consequence should reduce of the transient zone and increase the share of dispersed plug flow.

The results of simulations performed with two other turbulence methods – RANS and LES - have shown the differences for both investigated phenomena: flow field and temperature distribution. It has been shown that LES method indicate more particularly the fluid movement in regions of the tundish which are characterized with higher difference of the calculated variables.

Presented numerical simulations demonstrate the differences in the calculations of the tundish carried out using RANS and LES methods. In order to determine weather the models show similar results it was enough to make the calculations for one configuration of the tundish. The current model show slight difference in modeling using both methods. However, it is necessary to verify the obtained results based on the experimental data of industrial measurements (temperature measurements and RTD curves). Properly validated model can be used in the further study to analyze the impact of building the working space (flow modifiers) to remove the inclusions from steel and thus increase its purity.

Currently, studies on the impact of the LES method on the results concerning the characteristics of the RTD (along with verification of industrial data) in the tundish and non-metallic inclusions separation from liquid steel are performed.
### Nomenclature

| Symbol | Definition                        |
|--------|----------------------------------|
| $A$    | Van Driest constant (=26)        |
| $c_p$  | specific heat                    |
| $D_{eff}$ | effective diffusion coefficient |
| $D_m$  | molecular diffusion coefficient  |
| $D_t$  | turbulent diffusion coefficient  |
| $g_i$  | gravitational acceleration       |
| $k$    | turbulence kinetic energy        |
| $k_{eff}$ | effective thermal conductivity  |
| $k_p$  | turbulent kinetic energy at the first near-wall node |
| $m_t$  | mass of the tracer               |
| $p$    | pressure                         |
| $P$    | Prandtl number                   |
| $P_t$  | turbulent Prandtl number         |
| $q$    | wall heat flux                   |
| $S_{ij}$ | strain rate tensor               |
| $t$    | time                             |
| $\bar{t}$ | theoretical (mean) residence time |
| $t_{av}$ | mean residence time             |
| $T$    | temperature                      |
| $u$    | velocity                         |
| $u_{i,j}$ | velocity components             |
| $V$    | volume of liquid in the tundish  |
| $\mu$  | dynamic viscosity                |
| $\mu_{eff}$ | effective viscosity             |
| $\mu_t$ | turbulent viscosity             |
| $\nu$  | kinematic viscosity              |
| $\rho$ | specific density                 |
| $\rho_{st}$ | liquid steel density            |
| $\rho_{inc}$ | inclusion density               |

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### REFERENCES

[1] M. Warzecha, T. Merder, Metalurgija 52, 153-156 (2013).
[2] V. Singh, A.R. Pal, P. Panigrahi, ISIJ Int. 48, 430-442 (2008).
[3] R.K. Singh, A. Paul, A.K. Ray, Scand. J. Metall. 32, 137-147 (2003).
[4] L. Zhang, S. Taniguchi, K. Cai, Metal. and Mater. Trans. B 31, 253-268 (2000).
[5] H. Solhed, J. Alexis, U. Sjostrom, S.D. Yuan, L. Jonsson, Scand. J. Metall. 29, 127-238 (2000).
[6] L. Zhong, B. Li, Y. Zhu, R. Wang, W. Wang, X. Zhang, ISIJ Int. 47, 88-98 (2007).
[7] T. Merder, Materials Science Forum 654-656, 1557-1560 (2010).
[8] M. Warzecha, T. Merder, P. Warzecha, Metalurgija 53, 439-442 (2014).
[9] A. Robert, D. Mazumdar, Steel Res. Int. 72, 3, 97-105 (2001).
[10] A. Kumar, S.C. Koria, D. Mazumdar, ISIJ Int. 44, 12, 1217-1224 (2004).
[11] T. Zhou, M. Li, Q. Li, B. Lei, Q. Chenn, J. Zhou, Trans. Nonferrous Met. Soc. China 24, 1117-1124 (2014).
[12] D.Y. Sheng, L. Jonsson, Metal. and Mater. Trans. B 30, 979-987 (1999).
[13] L. Zhang, Steel Res. Int. 76, 11, 784-799 (2005).
[14] M. Javarek, P. Gittler, R. Roessler, B. Kaufmann, H. Presslinger, Steel Res. Int. 76, 1, 64-70 (2005).
[15] D.S. Kumar, T. Rajendra, A. Sarkar, R. Prasad, M. Ranjan, Iron&Steelmaking 36, 470-482 (2009).
[16] G. Luo-fang, L. Hong, L. Hai-tao, W. Yao, S. Wen-chen, Steel Res. Int. 20, 7-12 (2013).
[17] O.J. Illegbussi, ISIJ Int. 34, 732-746 (1994).
[18] K. Raghavendra, S. Sarkar, S.K. Ajmani, M.B. Denys, M.K. Singh, Applied Math. Modelling 37, 6284-6300 (2013).
[19] A. Kumar, S. Chakraborty, N. Chakraborti, Steel Res. Int. 78, 517-521 (2007).
[20] L. Chaoxiang, L. B Lao, Z. Shengyu, AASRI Procedia 3, 313-318 (2012).
[21] A. Najera-Bastida, L. Garcia-Demedices, P. Ramirez-Lopez, E. Torres-Alonso, R.D. Morales, Steel Res. Int. 78, 318-326 (2007).
[22] M. Warzecha, T. Merder, H. Pfeifer, J. Pieprzyca, Steel Res. Int. 81, 11, 987-993 (2010).
[23] J. Smagorinsky, Month. Wea. Rev. 91, 99-108 (1963).
[24] ANSYSFluent, User’s guide, version 14.0, Fluent Inc.

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