Supramolecular Self-Assembly as a Tool To Preserve the Electronic Purity of Perylene Diimide Chromophores

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Abstract: Organic semiconductors are promising for efficient, printable optoelectronics. However, strong excited-state quenching due to uncontrolled aggregation limits their use in devices. We report on the self-assembly of a supramolecular pseudo-cube formed from six perylene diimides (PDIs). The rigid, shape-persistent cage sets the distance and orientation of the PDIs and suppresses intramolecular rotations and vibrations, leading to non-aggregated, monomer-like properties in solution and the solid state, in contrast to the fast fluorescence quenching in the free ligand. The stabilized excited state and electronic purity in the cage enables the observation of delayed fluorescence due to a bright excited multimer, acting as excited-state reservoir in a rare case of benign inter-chromophore interactions in an excited multimer state that is in equilibrium with the excited singlet state. Our study shows rare cases of benevolent inter-chromophore interactions because of uncontrolled supramolecular assembly since one of the largest challenges yet to be overcome before organic molecules can replace the currently dominating crystalline inorganic semiconductors like silicon or gallium arsenide as future technologies based on plastic electronics.

Here we report a multi-chromophore system assembled in a fully controlled fashion using synthetic supramolecular chemistry based on coordination complexes. We design a pseudo-cube consisting of six tetratopic PDI-derivative molecules which self-assemble into a cage-like structure. Previous efforts in dye self-assembly resulted in the construction of mostly tetrahedral cages where the smaller inter-chromophore angles and distances gave rise to unfavorable electronic interactions and thus strong excited-state quenching. In contrast, the rigid framework and high structural stability of our cubic cage retain the electronic purity of the PDI chromophores, which is otherwise lost in the uncomplexed PDI ligands due to vibrational losses or π-stacking. The rich photophysics of the cage’s excited state, now stabilized through restriction of intramolecular rotation, reveals rarely observed benign inter-chromophore interactions, resulting in a hitherto unobserved emissive excited multimer state that is in equilibrium with the excited singlet to yield delayed fluorescence of the cage. Our study shows how supramolecular self-assembly provides a new platform to retain and control the electronic properties of well-conjugated chromophores have been known for centuries and are omnipresent, for example as photo-active molecules in photosynthesis or simply when used to dye fabrics for clothing. More recently, such dye molecules have been intensively studied for their optoelectronic properties in organic and molecular electronics applications, for example for organic photovoltaics (OPV) or organic light-emitting diodes (OLEDs), now commonly found in many displays when seeking high brightness and color-purity. Perylene diimide (PDI) represents such a prototypical chromophore molecule often used as structural motif for pigments or molecular electronics.

However, PDI, like the vast majority of highly conjugated planar aromatic compounds suffers from strong excited-state quenching and loss of its favorable electronic properties upon aggregation through π–π stacking, for example in concentrated solutions or thin films, or due to rovibrational losses. Such undesired inter-chromophore interactions because of uncontrolled supramolecular assembly present one of the largest challenges yet to be overcome before organic molecules can replace the currently dominating crystalline inorganic semiconductors like silicon or gallium arsenide as future technologies based on plastic electronics.

π-conjugated chromophores have been known for centuries and are omnipresent, for example as photo-active molecules in photosynthesis or simply when used to dye fabrics for clothing.[1,2] More recently, such dye molecules have been intensively studied for their optoelectronic properties in organic and molecular electronics applications, for example for organic photovoltaics (OPV) or organic light-emitting diodes (OLEDs), now commonly found in many displays when seeking high brightness and color-purity.[3,4] Perylene diimide (PDI) represents such a prototypical chromophore molecule often used as structural motif for pigments or molecular electronics.[5,6]

Introduction

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studied chromophores, providing a powerful route to bring molecular electronics applications in reach.

**Results and Discussion**

We first synthesize a suitably modified building block for subsequent supramolecular self-assembly based on the prototypical chromophore perylenediimide (PDI) by attaching phenylamine groups to the bay area and neopentyl groups to the head area for enhanced solubility (see Supporting Information for details on precursor synthesis). The thus modified PDI chromophore ligand L reacted with zinc(II) ions and picolinal to yield the supramolecular pseudo-cube C, formed from six such ligands (see Figure 1a).

We confirmed the cube-like cage structure by synchrotron-based single-crystal X-ray diffraction (Figure 1b). Importantly, the question arises to what extent this controlled supramolecular self-assembly impacts the optoelectronic properties of the PDI chromophore compared to the free ligand: Both H- and J-type exciton interactions could be hypothesized to occur, which could be favorable or unfavorable with respect to the photoluminescence (PL) of the resulting complex (Figure 1c).

We next investigate the steady-state optical properties of the cube-like PDI cage C and compare them with those of the free ligand L (Figure 2).

For the free PDI ligand L, we find significant electronic disorder leading to broadened absorbance features in its vibronic progression (Figure 2a). This energetic disorder initially increases upon increasing its concentration until at a certain threshold concentration the linewidth suddenly drops (see also Figure 2b), in conjunction with the occurrence of an additional absorbance feature around 330 nm. This is indicative of the onset of spontaneous aggregation of the ligand in solution. In contrast, we observe for the cage assembly C a very narrow linewidth throughout all tested concentrations, implying a high degree of electronic purity is achieved through the restriction of the PDI ligands’ motion, once confined as part of the cage. We see the far-reaching consequences of this energetic disorder in the free PDI ligand with respect to its emission properties (Figure 2c): Its photoluminescence (PL) is fully quenched (yellow line) with

![Figure 1. Synthesis and structure of the supramolecular pseudo-cube. a, Self-assembly of PDI ligand L into pseudo-cube C with only one of six ligands depicted for clarity. b, Structure of C as derived from synchrotron-based single-crystal X-ray diffraction. Counterions and co-crystallized solvent molecules are omitted for clarity. c, Relative orientation of possible PDI transition dipole moment couplings in the cubic cage.](image-url)
a PL quantum yield (PLQY) below our detection limit of $10^{-4}$ (see Supporting Information for details). We discuss the origin of this quenching in the context of rovibrational losses further below. In contrast, the cage assembly C (filled cyan area) shows significantly lower energetic disorder. b, Concentration-dependent 0–0 absorption peak linewidth of free ligand L and its cubic assembly C, quantifying the onset of uncontrolled aggregation in the ligand, in contrast to the unchanging high electronic order retained in C. c, Photoluminescence (PL) of dilute free ligand (yellow, fully quenched), highly concentrated aggregated ligand (purple, weak emission), and cage assembly (cyan, stronger emission like from pure PDI). Excited at 405 nm. d, Direct comparison between absorbance (red line), PL (cyan line) and PL excitation scan (PLE, red filled area) shows the narrow bands, clear mirror-symmetry, and high electronic purity of the PDI achieved in the cage assembly.

Figure 2. Supramolecular self-assembly as a tool for the controlled restoration of the electronic purity of PDI. a, Concentration-dependent absorbance of L with retrieval of sharp absorption peaks above a threshold concentration, when also an additional feature at 330 nm is observed, indicating aggregation. In contrast, the cage assembly C (filled cyan area) shows significantly lower energetic disorder. In stark contrast to these observations, for the cage self-assembly (cyan line) a much stronger PL was observed, showing an (about 100-fold) increased PL efficiency, even at low concentrations where electronic disorder and quenching prevails for the ligand.

This preserved electronic purity of the PDI emission in the cage as opposed to that in the free PDI ligand becomes even more obvious when directly comparing the cage absorbance and PL spectra (Figure 2d), showing near-perfect mirror symmetry between the spectra. For the uncontrolled PDI ligand aggregation (Figure 2c), the PL spectrum is instead truncated in its 0–0 peak and is indicative of H-type aggregation. The PL excitation scan (PLE, monitored at the emission center at 585 nm) of the cage also confirms the absence of any non-PDI core states that one could argue would influence the optoelectronic properties of the PDI upon self-assembly into the cage. Similarly, no additional low-energy absorbance tail is observed for the cage compared to a pure PDI molecule, confirming the absence of any unwanted extended conjugation between the PDI chromophores in the cage assembly that would impact its electronic purity. We also confirm that at higher concentrations the cage retains these electronically pure properties, and we show that changes to the PL spectrum at high concentrations can be described purely by accounting for self-absorption (see Supporting Information Figure S2), in contrast to the PL changes observed for the pure ligand upon uncontrolled aggregation, mentioned above.

Supramolecular self-assembly therefore serves here as a powerful tool to retain the electronic purity of its subcomponents. This would otherwise be lost when trying to functionalize a chromophore to make it useful for optoelectronic applications, for example shown in the restoration of the PL quantum yield.
otherwise lost in the ligand or only partially restored via its uncontrolled aggregation.

Having confirmed this, we now explore the excitonic properties of the pseudo-cubic chromophore cage compared to the free PDI ligand through time-resolved PL spectroscopy (Figure 3).

The measurements were performed using acetonitrile as solvent. In contrast to the fully quenched PL of the free ligand, we can observe rich photophysics in the excited state of the supramolecular PDI cube. This is a direct consequence of the strong restriction of intramolecular rotation in the cage-like self-assembly, whereas the free rotation of the phenylamine groups in the case of the free ligands leads to fast non-radiative decay to the ground state upon photoexcitation. Surprisingly, upon time-gating we not only observe an expected bright singlet emission of the cage, but also a spectrally well separated red-shifted and broad emission band centered around 640 nm (Figure 3a). We assign this feature to an “excited multimer state”, by which we mean a coupling of two or more of the chromophores in the cage in the excited state forming a new state. This is strongly reminiscent of the excimer emission observed before for covalently bound PDI-dimers and oligomers, for example, by the groups of Wasielewski (e.g. refs. [12, 13]) or Würthner (e.g. ref. [14] and citations therein). Importantly, this species forms only upon photo-excitation and subsequent electronic coupling of the chromophores with each other, followed by structural reorientation, explaining why this state is not observed in the steady-state absorbance spectrum shown earlier.

This observation is impressive in two ways: i) It is one of the very few examples of benign (favorable) rather than
malign (unfavorable) exciton-exciton interactions observed in a multi-chromophore system, where emission is usually fully quenched\(^{[15–17]} \)---we, for example, reported on full PL quenching in a chromophore-based tetrahedral cage\(^{[19]} \) rather than the 100-fold increase of singlet emission we observe in the present case. ii) We observe, to the best of our knowledge, for the first time an emissive excited multimer state in a supramolecular self-assembly of dye molecules, as a consequence of the preservation of the excited state due to the restriction of intramolecular rotational losses and the correct chromophore orientation in space, allowing for this favorable inter-chromophore coupling to take place. As we cannot determine directly the exact number of coupled chromophores in our system, we refer to this new state as excited multimer (\(E^*\) upon photo-induced formation, and structurally relaxing into state E), rather than as excimer (implying typically excited-state dimer, i.e. limited to only two chromophores).

Moreover, the kinetics of these excited states reveal a distinct delayed emission component for the singlet (Figure 3b–c), resembling those observed in thermally-activated delayed fluorescence emitters\(^{[19–21]} \) (see Supporting Information for modelling details). This is the result of the crossing and reverse-crossing between the bright singlet, the bright excited multimer, and—as we confirm below using transient absorption (TA) spectroscopy—a dark triplet state (Figure 3d). Both the excited multimer and the triplet are needed to explain all observed kinetics, and both can act as excitation reservoirs re-populating the singlet in a dynamic equilibrium, although we note that the majority of excitons in the self-assembly still ultimately decays non-radiatively, which we rationalize below using insights from TA and density functional theory (DFT). We also highlight the absence of any low-energy absorption onset for the cage UV/Vis spectrum (Figure 1d), further excluding the formation of any aggregates and related state hybridization in the cage’s electronic ground state.

Although a full computational characterization of the excited states of the cage was prohibitively computationally costly, time-dependent density functional theory (TDDFT) calculations on chromophore dimers extracted from the cage provide support for the existence of such an excited multimer (see Supporting Information Figure S8). These calculations show coupled excited states at energies that match very well those found experimentally corresponding to the \(E^*\) to \(E\) transition shown in Figure 3d (at around 650 nm); corrections due to the lack of interactions with other molecules, and the limitations of the level of theory applied, would also be expected, but will act in opposite directions, leading to a cancellation of errors. The coupling between excited states is strongest for ligands on adjacent perpendicular faces of the cube, but is still present for ligands on opposite parallel faces.

We now confirm these photophysical processes in the cage and their absence in the free ligand by employing TA spectroscopy, which allows us to also resolve non-emissive species (Figure 4).

The transient absorption data shows the changes in absorbance of the material after initial excitation with a pulsed pump beam (400 nm for the ultrafast measurements) and mapped across different time delays between the pump and the broadband probe beam, measured in transmission (T). For the pure PDI ligand in solution (Figure 4a), we find a positive change in transmission signal from around 450–570 nm which can be assigned to the ground-state bleach (GSB) of the \(S_0\) to \(S_1\) transition, and a broad negative signal from about 600 nm onwards, which corresponds to overlapping photo-induced absorption (PIA) peaks from the \(S_1\) state into higher lying states and, upon ultrafast intersystem crossing, from \(T_1\) into higher lying states.\(^{[22, 23]} \) Figure 4b shows spectrally integrated kinetics of these transitions, revealing that the entirety of the excited state population of the free ligand decays back to the ground state with an average mono-exponential lifetime of 18 ps, much faster than the nanosecond radiative lifetime of PDI, explaining why the PL of the ligand is fully quenched.

In contrast, for the supramolecular cage assembly the excited-state lifetime extends far into the ns-regime, in line with the rich emission properties discussed above. For the PDI cage, the TA spectrum (Figure 4c, d) also shows modified spectral features in the region of the vibronic progression of the GSB, as in this bright emitter stimulated emission (SE) can be observed as a positive change in transmission signal at early times. Figure 4e demonstrates how the early time TA spectrum of the cage can be well understood in terms of a superposition of its absorbance and emission properties. At ns-time delays (not measurable for the PDI ligand which is fully relaxed back to the ground state by then) for the cage we moreover see a broad positive signal around 650 nm (Figure 4d), which matches well the excited multimer emission observed in the PL experiments. We anticipate this to be a SE feature of the excited multimer convoluted with the PIA (now decreased in intensity) in this region—as this excited multimer state only forms delayed after photo-excitation it explains why this signal is absent in the early time TA data. Aside from the fact that the triplet state in PDI molecules is well reported in the literature,\(^{[22]} \) we also note that in order to fit all kinetics of the PDI cage (i.e. ns-iCCD & ps-TCSPC PL data and ns- & fs/ps-TA data) do we need to include both the dark triplet state and the bright excited multimer state in the model (see Supporting Information for details).

To further understand our experimental results, we performed first principles calculations, examining the excitations of the PDI ligand with its phenylamine linkers using time-dependent density functional theory (TDDFT). In particular, we investigated the excitations for several dihedral angles between the phenyl-ring moieties and the PDI core (Figure 5).

We calculated the absorption spectra of the PDI ligand \(L\), using the highly accurate OT-LRC-omegaPBE functional,\(^{[24, 25]} \) as a function of the rotation angle of the phenylamine rings (Figure 5f). The positions of the two strongest absorption peaks at around 450 and 500 nm compare very well with the experimental absorption data shown earlier in Figure 2. The peak at around 500 nm is largely unaffected by the dihedral angle, whereas the peak at around 450 nm dramatically decreases in strength as the angle increases, implying a
strong coupling to the rotation of the phenylamines. This coupling is further explored by examining the difference density for the 450 nm excitation at the various dihedral angles, as shown in Figure 5a–e. This shows that the character of the excitation is also strongly dependent on the dihedral angle. At low angles, the excitation is largely localized on the PDI core, but at higher angles, the phenylamine rings become more involved, acting as electron donors, with the excitation taking on a stronger charge transfer character. This charge transfer character makes radiative recombination less likely, and correlates with the decrease in the oscillator strength with increasing dihedral angle, as seen in Figure 5f.

We further quantify the coupling of this excitation with the rotation of the ligands by calculating the non-adiabatic coupling vector (NACR), which provides a measure of the coupling between electronic excitation and atomic motion. We calculated the coupling between the excitation at around

Figure 4. Confirmation of excited multimer and triplet dynamics in the supramolecular PDI cage with transient absorption (TA) spectroscopy, unravelling the rare case of benign inter-chromophore interaction in a supramolecular assembly, where the triplet and excited multimer states act as reservoirs for delayed luminescence. a, ps-TA spectra of PDI ligand L and b, kinetics showing excited-state quenching with a lifetime of 18 ps for the free ligand, but largely extended lifetimes for the cage. We note that the spectral indent at 800 nm is due to residual 800 nm laser scatter which is used to generate pump and probe beams in the lab. c, ps- and d, ns-TA spectra for the PDI cage C, showing an extended excited-state lifetime into the ns-range and the emergence of the positive excited-multimer stimulated-emission band around 650 nm at later times for the cage. e, The early time TA spectrum of the PDI cage can be well reconstructed from the contributions from its absorbance (ground-state bleach) and early time PL (stimulated emission), the latter of which is absent in the ligand TA spectrum when comparing a and c, as all emission is quenched for the ligand. See Supporting Information for experimental details and fitting procedure.
450 nm and two sets of atomic motion: i) the rotation of a ligand, and ii) a breathing mode of the PDI core, which is also relevant to the relaxation from the equilibrium geometry in the ground state to that in the excited state (see Supporting Information for computational details). We find that the coupling of the electronic excitation to the rotation of the ligands is 6.7 times stronger than to the PDI breathing mode, demonstrating that there is a strong coupling between the excitation and the rotation of the ligands. This is further demonstrated by optimizing the geometry of the system in the excited state corresponding to the 450 nm excitation. Importantly the excited state equilibrium geometry has a larger dihedral angle between the phenylamine ligands and the PDI core than the ground state equilibrium geometry (49° vs. 51°). Although this change in angle is small, we expect it to be an underestimate of the true effect, as the PBE functional, which has known issues with describing charge transfer, was used for the excited-state geometry optimization for reasons of computational cost. Together with the results of the NACR computation, this provides strong evidence that there is a strong coupling between rotations of the ligands and the excitations, which is responsible for the non-radiative losses in the free molecule. Restriction of this rotation in the supramolecular cage thus explains the observed enhancement in luminescence compared to the free PDI ligand.

Our calculated energetic positions of the $S_1$ state at 2.46 eV and the $T_1$ state at 1.18 eV for the free PDI ligand, respectively (2.47 eV and 1.13 eV in the cage geometry for each case), also match very well the positions determined experimentally from the PL (singlet feature) and TA (singlet and triplet features).

Taken all together, the computational results imply that electronic excitations couple strongly to the rotation of the phenylamine ligands relative to the PDI core, providing a route for non-radiative energy loss and recombination. Simultaneously, exciting the system leads to the dihedral angle relaxing towards a larger dihedral angle, which is associated with a decrease in oscillator strength, making radiative recombination less likely. This provides an explanation for the quenching of photoluminescence in the free molecule. In the cage, however, the ligands are not free to rotate. The ground state dihedral angle between the PDI core and phenylamine ligands is much larger in the cage than in the free molecule, meaning that the oscillator strength is weak (though non-zero), but non-radiative recombination via coupling to ligand rotation is no longer possible. This allows radiative recombination to become competitive, producing the observed increase in photoluminescence, and extending the excited state lifetime to allow for the inter-chromophore coupling induced excited-multimer emission to be observed in the supramolecular cage.

We also note that the out-of-plane twisted configuration of the phenyl rings with respect to the PDI core results in a more pronounced CT character of the excited state for the
PDI ligand, which would in principle facilitate inter-system crossing to form triplets on ultrafast timescales. This would explain the loss of PL we observe for the PDI ligand, but would not explain the fast excited state decay within 18 ps that we observe in TA (the triplet state would be long-lived). Instead, due to the strong non-radiative losses resulting from the coupling to the ring rotations, all excitations are ultimately quenched non-radiatively in the case of the free ligand, as also supported by our calculations. In contrast, the restriction of intramolecular rotation in the cage assembly leads to the successful recovery of the intrinsic optical properties expected from the pure PDI ligand, i.e. it shows both intersystem-crossing to form triplets, emission from its excited singlet state (which has still significant CT character and reduced oscillator strength triplets), and, importantly, an excited-multimer emissive state which acts as an excitation reservoir for observing delayed emission.

**Conclusion**

In summary, we report on the synthesis of a supramolecular pseudo-cube formed from modified PDI dye molecules. We find this cage assembly to show 100-fold enhanced emission compared to its free PDI ligand subcomponent and that the rigid cage framework acts as a powerful tool to retain the electronic purity of the chromophores which is typically lost in uncontrolled aggregation. The suppression of non-radiative vibrational losses allows for the observation of an emissive excited multimer state through benign interchromophore coupling enabled by the high level of assembly control, paving the way for tailored optoelectronic applications following chemical bottom-up design.

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**Conflict of Interest**

The authors declare no conflict of interest.

**Data Availability Statement**

The data that support the findings of this study are openly available from the University of Cambridge online data repository at https://doi.org/10.17863/cam.93575.

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