Modeling $\delta^D-\delta^{18}O$ Steady-State of Well-Sealed Perennially Ice-Covered Lakes and Their Recharge Source: Examples From Lake Untersee and Lake Vostok, Antarctica

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Perennially ice-covered lakes that are tightly sealed from the atmosphere represent a unique group of polar lakes. In these lakes, the $\delta^D-\delta^{18}O$ evolution of the water column and steady-state conditions are controlled by rates of recharge and freezing at the bottom of the ice cover. We developed a recursive model (FREEZCH9) that takes into account the changing salinity in the water column as a result of freezing and mixes the recharge water to the residual water in well-sealed perennially ice-covered lakes. Our model is tested against datasets from Lake Vostok and is used to assess the $\delta^D-\delta^{18}O$ mass balance of Lake Untersee and evaluate if the lake is in isotopic steady-state. Our FREEZCH9 simulations fit well with the predicted $\delta^D-\delta^{18}O$ values of Lake Vostok’s upper water column and the overlying accreted ice. Simulations with FREEZCH9 also suggests that Lake Untersee is in isotopic steady-state and that its two input sources (i.e., subaqueous terminus melting of the Anuchin Glacier and subglacial meltwater) have similar $\delta^D-\delta^{18}O$ composition. Our modeling demonstrates that Lake Untersee most likely did not receive additional input from surface streams during the last 300–500 years. FREEZCH9 may be also used to determine if any groundwater systems of the McMurdo Dry Valleys are fully or partially recharged by subglacial lakes.

Keywords: isotope geochemistry, freezing, ice-covered lakes, Antarctica, FREZCHEM

INTRODUCTION

In Antarctica, several hundred lakes have been identified and classified according to their ice cover regime (Figure 1A; Morgan et al., 2007; Vincent et al., 2008). Seasonally ice-covered lakes are found along the warmer Antarctic Peninsula and other coastal regions. These lakes lose their ice cover in austral summer and are typically recharged by a combination of local precipitation and glacial meltwater (e.g., Gibson, 1999; Lyons et al., 2013). Perennially ice-covered lakes are found in polar desert regions and exist as two main types: those that develop moats in summer and are fed by glacial melt streams, and those that are tightly sealed from the atmosphere and solely fed by subaqueous
FIGURE 1 | (A) Distribution of surface snow \( \delta^{18}O \) values across Antarctica (data from Touzeau et al., 2016). (B) Stable water isotope (\( \delta D-\delta^{18}O \)) ratios of perennially ice-covered lakes in the Antarctic: Princess Astrid Coast (Lake Untersee), Southern Victoria land region (Lake Miers, Lake Vanda, Lake Bonney, Lake Fryxell, Lake Vida) (Matsubaya et al., 1979; Miller and Aiken, 1996; Dugan et al., 2015) and Soya Coast (Skallen Oike) (Matsubaya et al., 1979). AMWL, Antarctic Meteoric Water Line from Masson-Delmotte et al. (2008) (\( \delta D = 7.75 \delta^{18}O - 4.93; r^2 = 0.99; \) Masson-Delmotte et al., 2008).
column that includes the evolution of the ice-water isotope fractionation factor as freezing changes the salinity of the residual water and recursive recharge that mixes with the residual lake water.

The objective of this study is to develop a model of δD-δ18O evolution of well-sealed perennial ice-covered lakes that accounts for changing chemistry in the residual water and annual recharge that mixes with residual water. This objective was achieved by using FREEZCH5, an isotope-augmented version of the FREZCHEM low temperature geochemistry model (Marion et al., 2010; Fisher et al., 2020) and making the model recursive. The model is tested against datasets from Lake Vostok and is then used to assess the δD-δ18O mass balance of Lake Untersee and evaluate if the lake is in isotopic steady-state. The results are presented in terms of residence times of water with different mixing scenarios, which allow to apply the findings to other well-sealed perennial ice-covered lakes or subglacial lakes.

MATERIALS AND METHODS

Background on Water-Ice Fractionation During Freezing

The freezing of water under equilibrium condition follows a Rayleigh-type fractionation:

\[ R = R_{0f}(\alpha_{i-w} - 1) \]  

where \( R \) is the isotope ratio of \(^{18}\)O/\(^{16}\)O or D/H and of \( \alpha_{i-w} \) is the water-ice fractionation factor with two distinct sets of \( \alpha_{i-w} \) for \(^{18}\)O/\(^{16}\)O and D/H reported in the literature: 1.0031 and 1.0193, respectively (O’Neil, 1968); 1.0028 and 1.0206, respectively (Suzuoki and Kimura, 1973).

During freezing, the forming ice is \(^{18}\)O enriched but the presence of residual water if the water activity calculated from \( h \) is the thickness of the boundary layer (cm), \( v \) is the freezing rate (cm s\(^{-1}\)), \( D^* \) is the diffusion coefficient in water. At 0°C, \( D^* \) values for \( H_2^{18}\)O and HDO are 1.1 \( 10^{-5} \) cm\(^2\) s\(^{-1}\) and 1.33 \( 10^{-5} \) cm\(^2\) s\(^{-1}\), respectively (Wang et al., 1953).

When the freezing rate is slower than the diffusion coefficient, \( \alpha_{FR} \) approximates the equilibrium fractionation factor, but under increasing freezing rate, \( \alpha_{FR} \) is reduced towards unity (i.e., Lacelle, 2011).

Description of FREEZCH5 (Isotope-Augmented FREZCHEM)

The core of the FREEZCH5 model is FREZCHEMv15, an equilibrium chemical thermodynamic model over the temperature range of −73 to 25°C (Marion and Kargel, 2008; Fisher et al., 2020). FREZCHEM simulates the freezing of water by decreasing the temperature in fixed steps and determines the presence of residual water if the water activity calculated from the Pitzer equations is less than the equilibrium constant for water-ice. At each decreasing temperature step ("i"), the model provides: (1) the amount of residual water (in g; \( \text{WAT}_{i,0} \)); (2) the amount of ice formed (in g; \( \text{ICE}_{i,0} \)); (3) the molalities of the major cations (\( \text{Na}^+, \text{Ca}^{2+}, \text{Mg}^{2+}, \text{K}^+ \)) and anions (\( \text{Cl}^-, \text{NO}_3-, \text{SO}_4^{2-} \)); (4) the amount of hydrated salts that precipitates (in g; \( \Delta \text{WAT}_{\text{Na}}, \Delta \text{WAT}_{\text{Mg}}, \Delta \text{WAT}_{\text{Ca}} \)); and (5) the total ionic strength of the solution (proportional to conductivity and salinity of the residual water). FREEZCHEM completely segregates the solutes in the residual water and none are incorporated as inclusions in the ice lattice or along grain boundaries and likely over-estimates the salinity in the residual water (i.e., Killawee et al., 1998; Petrenko and Whitworth, 1999). However, properly accounting for ionic segregation in equilibrium modeling is challenging as it was found that the concentration factor (or the segregation coefficient) is dependent on initial water chemistry and freezing rates (Santibáñez et al., 2019).

The evolution of δ\(^{18}\)O of the residual water (δ\(^{18}\)Orw) and for the incremental ice that forms at each decreasing temperature step was added to FREZCHEM in a routine called FREEZCH5, where the initial δ\(^{18}\)O composition of the water and the \( \alpha_{i-w} \) is
where \( \delta^{18}O_{rw} \) is the ice-water fractionation factor (corrected for initial isotopic composition using equation 1), \( \alpha^{18}O_{w-Mgprecip} \) is the water-MgCl\(_2\) precipitate fractionation coefficient; \( \alpha^{18}O_{w-MgCl2} \) is that for water-MgCl\(_2\): 12H\(_2\)O; and \( \alpha^{18}O_{w-CaCl2} \) is CaCl\(_2\)-6H\(_2\)O. Note that \( \delta^{18}O_{rw} \) is the isotopic composition for the total water in the solution (free water and the water attached in the hydration spheres around the positive ions).

The various hydrated salts do not have reported water-precipitate fractionation factors and we assume that they are unity or as defined by Sofer and Gat (1972, 1975) for the cations-hydration spheres within the liquid solution. Since FREZCHEM is an equilibrium model, the effect of freezing rates on water-ice fractionation factors are not included, but these should have little effect on the freezing of perennially ice-covered lakes where freezing takes place near 0\(^\circ\)C at the ice-water boundary.

With \( \delta^{18}O_{rw} \), we can use the Sofer and Gat (1972, 1975) isotope salt effects correction to determine the \( \delta^{18}O \) offset between the \( \delta^{18}O \) total water (free and hydration sphere waters) and \( \delta^{18}O \) free water only (i.e., water activity), a correction that depends on the molality of each cation (Na\(^{+}\), Ca\(^{2+}\), Mg\(^{2+}\), K\(^{+}\)):

\[
(\delta^{18}O_{rw} - \delta^{18}O_{activity}) = \Delta \delta^{18}O_{Na^{+}} + \Delta \delta^{18}O_{Mg^{2+}} + \Delta \delta^{18}O_{Ca^{2+}} + \Delta \delta^{18}O_{K^{+}}
\]

where \( \Delta \delta^{18}O_{cations} \) are functions of the remaining liquid water molality, which are calculated at each temperature step. The FREEZCH5 model is described in detail in Supplementary Appendix A of Fisher et al. (2020).

### Description of FREEZCH9 (a Recursive FREEZCH5)

For perennially ice-covered lakes under hydrological steady-state condition, the annual rate of water freezing at the bottom of the ice cover equals the annual ablation rate at the ice surface (Wilson and Wellman, 1962; McKay et al., 1985). This implies that to maintain the lake water volume constant (\( \Delta V = 0 \)), the annual accretion and ablation rates of the ice cover must be equal. We developed a recursive version of FREEZCH5 (FREEZCH9) that maintains \( \Delta V = 0 \) by mixing the evolved chemistry and \( \delta D-\delta^{18}O \) composition of the residual water with an input of water of fixed chemistry and \( \delta D-\delta^{18}O \) composition, which then produces the new input chemistry and \( \delta D-\delta^{18}O \) for the next loop. The hydrated precipitates that may form are accumulated in the series. Supplementary Appendix A provides details of FREEZCH9.

### Field Sampling and Laboratory Analysis

The water column in theoxic basin of Lake Untersee was sampled in December 2016 at 10-m depth interval using a 2.2-L acrylic Kemmerer bottle content and samples were stored in sealed 20 ml high density polyethylene bottles (HDPE) bottles. The ice cover was sampled at the same location in December 2017 with a Cold Regions Research and Engineering Laboratory coring kit to a depth of 2 m to prevent mixing with lake water. Surface samples from the Anuchin Glacier were collected with a Kovacs ice corer powered by a Bosch Hammer GBH 36V-LI PLUS electrical drill, to a depth of 50 cm (e.g., Weisletten er et al., 2019). Samples from the Anuchin Glacier and the ice cover of Lake Untersee (sliced at 2 cm intervals) were melted in sealed Ziploc bags, transferred in HDPE bottles and shipped in coolers to the University of Ottawa where they were stored at 4\(^\circ\)C until analyzed for stable water isotopes.

The \( ^{18}O / ^{16}O \) and D/H ratios of lake water and melted ice samples were analyzed using a Los Gatos Research liquid water analyzer coupled to a CTC LC-PAL auto sampler and verified for spectral interference contamination. The results are presented using the \( \delta \)-notation (\( \delta^{18}O \) and \( \delta D \)), where \( \delta \) represents the parts per thousand differences for \( ^{18}O / ^{16}O \) or D/H in a sample with respect to Vienna Standard Mean Ocean Water (VSMOW). Analytical reproducibility for \( \delta^{18}O \) and \( \delta D \) was \( \pm 0.3\% \) and \( \pm 1\% \), respectively. Deuterium-excess (\( \delta D \)) was then calculated using the following equation (\( \delta D = \delta D - 8 \delta^{18}O \); Dansgaard, 1964).

### RESULTS

#### Modeling the Freezing of Low to High Salinity Waters

The freezing point of water is determined by the chemical composition of the solution and ranges from 0\(^\circ\)C for pure water to -2.3\(^\circ\)C for sea water (Figure 2A). Freezing under equilibrium conditions progressively decreases the amount of residual water while increasing the concentration of solutes in the residual water. This cryo-concentration of solutes on decreasing residual water is dependent on the initial chemical composition of the solution where for nearly pure water the bulk of the water is frozen over the 0 to -4\(^\circ\)C range, but for more saline waters, c. 15-20\% of residual water may occur over the -5 to -20\(^\circ\)C range (Figure 3A). For brackish to saline waters, hydrated salts can precipitate (NaCl-2H\(_2\)O at -23\(^\circ\)C, MgCl\(_2\)-12H\(_2\)O at -36\(^\circ\)C) and the formation of these precipitates further reduces the amount of residual water (Figure 2A).

The dependence of the initial chemical composition of the solutions on the amount residual water is reflected in the \( \delta^{18}O \) of the residual water (Figure 2B). For nearly pure waters, the \( \delta^{18}O \) of the residual water rapidly decreases as most of the water freezes over a narrow temperature range. For example, the freezing of nearly pure water with an initial \( \delta^{18}O \) composition of -35\% over the temperature range of 0 to -4\(^\circ\)C will cause the \( \delta^{18}O \) of the residual water to rapidly decrease to value of -45\% (when residual water fraction is 0.05). In contrast, the freezing...
of sea water with the same initial $\delta^{18}$O composition over the temperature range of 0 to $-4^\circ$C will cause the $\delta^{18}$O of the residual water to decreases to $-37\%$ (when residual water fraction is 0.85). A value of $-45\%$ in the residual water of sea water would only be reached following the precipitation of NaCl·2H2O.

These numerical simulations allow us to explore the effect of temperature on residual water content and its $\delta^{18}$O composition during equilibrium freezing of solutions with varied salinities. However, exploring the evolution of $\delta^{18}$O of residual water as a function of decreasing fractions of residual water revealed no significant differences between solutions of varying salinities (Figure 2C). As such, a Rayleigh-type isotope fractionation during equilibrium freezing of liquid water with varied salinities using FREEZCH5 shows that, as freezing begins, the first ice to form will be enriched in $\delta^{18}$O by about 3% (and about 20% in $\delta^D$), but as freezing continues, the $\delta^{18}$O composition of the ice formed progressively becomes depleted as the $\delta^{18}$O composition of the residual water trends toward lower value. The extent of $\delta^{18}$O depletion of the residual water during freezing is constrained by the evolving eutectic temperature of the residual water and temperature at the ice-water interface. Despite little differences in the evolving $\delta^D$-$\delta^{18}$O of residual waters of varied salinities, a difference is observed in the $\delta^D$-$\delta^{18}$O composition of the forming ice following the precipitation of hydrated minerals (Figure 2D).
TABLE 1 | Initial hydrochemical parameters for the mixing simulations.

| Parameter | Initial D/H | Initial δD | Initial δ18O | Initial P(D) | Initial P(18O) |
|-----------|-------------|------------|--------------|--------------|---------------|
| 100% Sea water | 3.1 | 19.3 | 19.3 | 19.3 | 19.3 |
| 50% Sea water | 3.1 | 19.3 | 19.3 | 19.3 | 19.3 |
| 25% Sea water | 3.1 | 19.3 | 19.3 | 19.3 | 19.3 |

For perennially ice-covered lakes under hydrological steady-state, the evolution of δ18O in lake water and ice during equilibrium freezing was explored using FREEZCH9 for a range of recharge and mixing scenarios (Figure 3). The results are expressed in terms of residence times instead of annual loops to facilitate comparison. For all mixing scenarios, the results show that isotopic equilibrium (steady-state) in the lake water and ice is reached after more than three residence times. However, the difference between δ18O of input water and that of isotopic equilibrium decreases under increasing mixing scenarios. For mixing scenarios <~5%, the Δδ18O input and equilibrium approaches ln(α18Ow); however, as the amount of annual mixing approaches 95%, the Δδ18O input and equilibrium approaches 0.

Testing FREEZCH9 With Lake Vostok, East Antarctic Plateau

Lake Vostok is a large subglacial lake located beneath c. 4 km of ice on the east Antarctic plateau (Lyons et al., 2016). The lake is about 250 km long and 80 km wide, has a surface area of ~13,000 km² and a water volume of 4658–6350 km³ depending on the estimation method (e.g., Studinger et al., 2004; Siegert et al., 2011; Li et al., 2019). Lake Vostok is recharged from the melting of the overlying East Antarctic Ice Sheet in the northern basin (incoming rate of c. 4 cm yr⁻¹) and loses ice via ice accretion at the ice-water interface in the southern and central basins (freezing rate of c. 2 cm yr⁻¹) (Suzuoki and Kimura, 1973; 2002; Studinger et al., 2004). The annual input of water is estimated at 0.19 km³ yr⁻¹, which translates to a residence time equivalent to c. 28,000 years or an annual mixing rate of c. 0.0037% (Royston-Bishop et al., 2004).

Based on the average of δ18O time-series during the last four glacial cycles in the Dome B record, Royston-Bishop et al. (2004) first estimated the δD–δ18O of input water to Lake Vostok to be −442.2 and −56.7‰, respectively. Lipenkov et al. (2016) later revised the δD–δ18O composition of input water, based on data from the overlying accreted ice, to be −442.4‰ and −56.2‰, respectively, with D-excess of 7.2‰. Based on a closed-system isotopic equilibrium model using the δD–δ18O data of re-frozen lake water in borehole, Ekaikin et al. (2016) estimated the average δD and δ18O composition of the Lake Vostok to be −455 ± 1‰ and −59.0 ± 0.3‰, respectively (D-excess of 17 ± 1‰).

FREEZCH9 was used with input parameters defined as 0.0037% annual mixing (e.g., Royston-Bishop et al., 2004), the average major ions concentrations in the Vostok ice core which extends to 160 kyr BP (Legrand et al., 1988), and the equilibrium factors (αw−i) of O'Neil (1968) and Suzuoki and Kimura (1973) also corrected for initial isotope composition of water. When using the δD–δ18O of the input water estimated by Royston-Bishop et al. (2004) (~−442.2 and ~−56.7‰, respectively), the model does not perfectly match the measurements in the accreted ice (Figure 4). However, if we use the αw−i corrected for initial isotope composition of water and adjust the δD–δ18O of input water to match the measurements in the accreted ice, we find input values for δD–δ18O of −443.5 and −56.4‰,
respectively. With 0.0037% annual mixing, the time for the water column to reach isotopic equilibrium is in the order of 2–3 residence times and the δD-δ18O of Lake Vostok is estimated to be −453.5 and −59.1‰, within error of the values reported by Ekaykin et al. (2016).

FREEZCH9 and Lake Untersee, Dronning Maud Land, Antarctica

Lake Untersee is a perennially ice-covered lake located in the Gruber Mountains of central Dronning Maud Land, approximately 90 km southeast of the Schirmacher Oasis. The 6.5 km long and 1.5 km wide lake (surface area = 8.73 km²), with a water volume of $5.21 \times 10^8$ m³, is located in a closed-basin dammed at its northern end by the Anuchin Glacier (Faucher et al., 2019). Lake Untersee has two subbasins: (1) a large well-mixed oxic basin at the northern and central section with a maximum depth of 169 m; and (2) a shallower basin at its southern section with a maximum depth of 100 m depth (Wand et al., 1997; Andersen et al., 2011). Unlike most perennially ice-covered lakes, Lake Untersee does not develop a summer moat. Loss of water is entirely through the sublimation of the ice cover (61 ± 11 cm yr⁻¹) with annual loss of $4.90 \pm 0.8 \times 10^6$ m³ of water (or 0.94 ± 0.17% of total lake water volume) (Faucher et al., 2019). To maintain hydrological steady-state, Lake Untersee receives an equal volume of inflow sourced from the subaqueous melting of the Anuchin Glacier (40–45% of annual contribution) and from subglacial meltwater (55–60% of annual input) (Faucher et al., 2019).
The oxic water column of Lake Untersee has a narrow δD-δ¹⁸O composition, from −288.4 to −287.3‰ and from −37.9 to −37.6‰, respectively (Figure 5). With D-excess ranging from 12.8 to 14.7‰, the water samples are distributed above the AMWL (Figure 5). The ice cover sampled at the same location has higher δD-δ¹⁸O values varying from −279.5 to −268.5‰ and from −36.2 to −33.55‰, respectively, with lower D-excess ranging from −8.8 to 11.4‰ (Figure 5). FREEZCH9 was used with input parameters defined as 1% annual mixing (Faucher et al., 2019), α_i−w of O’Neil’s (1968) and Suzuoki and Kimura’s (1973) corrected for initial isotope composition of water and the δD-δ¹⁸O of input water was adjusted to match the δD-δ¹⁸O measurements in the oxic water column. The initial chemistry of the input water was based on data from nearby shallow firn core (Isaksson et al., 1996). The FREEZCH9 modeling indicates that the measured δD-δ¹⁸O values in the water column is in isotopic equilibrium with initial input water having δD-δ¹⁸O values of −275.0 and −35.0‰, respectively. With 1% annual mixing, the time to reach isotopic equilibrium in the water column is in the order of c. 300–500 years.

DISCUSSION

δD-δ¹⁸O Composition of Input Waters to Lake Untersee

Based on a hydrological and energy mass balance, it was suggested that the well-sealed perennially ice-covered Lake Untersee is recharged by two sources: subaqueous terminus melting of the Anuchin Glacier (40–45% of annual contribution) and from subglacial meltwater and/or from groundwater (55–60% of annual input) (Faucher et al., 2019). The FREEZCH9 modeling using 1% annual recharge and mixing with lake water suggests that the δ¹⁸O composition of Lake Untersee (−37.9 to −37.6‰) is in equilibrium with source waters having an average δ¹⁸O composition of −35.0‰. The δ¹⁸O composition of
the contribution from the subaqueous melting of the Anuchin Glacier can be estimated from the thickness of the glacier at the lake-glacier interface (c. 160 m) and the age-depth relation from the Dome Fuji, Dome C, and Taylor Dome ice cores (Lorius et al., 1979; Steig et al., 2000; Uemura et al., 2012). The age of the ice in the uppermost c. 160 m at these three sites varies from 0 to 3000–4500 years (Figure 6A); assuming a similar age-depth relation applies for the Dronning Maud Land region, the average age of the subaqueous meltwater recharging Lake Untersee is estimated at c. 1800 years. The $\delta^{18}O$ composition of a series of shallow ice cores (uppermost 50 cm) of a 3.2 km long transect on both sides of the medial moraine on the Anuchin Glacier ranged from $-36.4$ to $-30.8\%$ (average of $-34.2 \pm 1\%$). Given that over the past 3000–5000 years, the $\delta^{18}O$ time-series of deep ice cores showed fluctuations in the order of $0.5\%$, the average $\delta^{18}O$ of near-surface ice of the Anuchin Glacier likely reflects that over a 160 m thick section (or past c. 1800 years). Therefore, the $\delta^{18}O$ of Lake Untersee is in equilibrium with subaqueous melting of the Anuchin Glacier having an average $\delta^{18}O$ composition of $-34.2 \pm 1\%$ and to obtain the calculated $\delta^{18}O$ of input water of $-35.0\%$, a two-component mixing model indicates that the subglacial meltwater has an average $\delta^{18}O$ composition of $-35.8 \pm 1\%$ ($\delta D: -280\%$; D-excess: 6%). Considering that the $\Delta \delta^{18}O$ of last glacial maximum to Holocene age glacier ice is in the order of 6–8\%, the subglacial meltwater recharging Lake Untersee is likely of similar age (late Holocene) to that of the Anuchin Glacier and does not reflect subglacial meltwater sourced during the last glacial period or far in the Antarctic interior.

The oxic water column of Lake Untersee is well-mixed as a result of buoyancy-driven convection which allows for effective mixing within a time-scale of one month (Steel et al., 2015). Based on the volume of water in the lake, its surface area and ablation rate, the residence time of water in the lake was estimated at c. 100 years (Faucher et al., 2019) and $\delta^{18}O$ steady-state is achieved within 300–500 years (3–5 residence times). Considering that the 2016 water samples in Lake Untersee plot above the AMWL with D-excess of 14\%, this suggest that for at least the past 300–500 years: (1) subaqueous melting of the Anuchin Glacier and subglacial meltwater were the only sources of water recharging the lake (i.e., no to very little recharge from surface streams with an evaporated $\delta^{18}O$ signature); (2) the $\delta D-\delta^{18}O$ composition of the subglacial meltwater is likely distributed on the AMWL and does not reflect a subglacial meltwater that has evolved under cryo-freezing; and (3) the ice cover has remained well-sealed to atmospheric exchange (i.e., no evaporative loss of the water column). These conditions were likely made possible by the cooler air temperatures in the region since the 1800s (Isaksson et al., 1996).

Despite generally cooler temperatures over the past few hundred years, we can test for the effect of an anomalous warm summer on the potential contribution of surface stream to the $\delta D-\delta^{18}O$ composition on Lake Untersee. As a hypothetical scenario, we mixed 5–10\% input of stream having a $\delta D = -233.0\%$ and $\delta^{18}O = -23\%$ (a scenario that represents the Anuchin Glacier $\delta D-\delta^{18}O$ composition that evaporated 40\% under relative humidity of 50%) with Lake Untersee and the $\delta D-\delta^{18}O$ composition of the lake evolved outside the range measured in the oxic water column (10%mix: $\delta D = -281.5\%$; $\delta^{18}O = -36.4\%$; 5%mix: $\delta D = -284.7\%$; $\delta^{18}O = -37.1\%$). If Lake Untersee then continues to be under hydrological steady-state and keeps being recharged by subaqueous melting and subglacial meltwater sources having an average $\delta^{18}O$ composition of $-35.0\%$, the $\delta D-\delta^{18}O$ of Lake Untersee will evolve to the isotopic steady-state determined by input and recharge over a period of 200–300 years. Therefore, this modeling exercise shows...
that Lake Untersee most likely did not receive additional input from streams under an anomalous warm summer as its δD-δ18O composition would be distributed closer to the AMWL.

**Application of FREEZCH9**

This study developed an isotope-augmented version of FRESCHM (FREEZCH5) and made it recursive (FREEZCH9) to predict the δD-δ18O evolution and isotopic steady-state of well-sealed perennially ice-covered lakes and subglacial lakes. The model accounts for changes in the ice-water isotope fractionation factor as freezing increases the salinity of the residual water and, to maintain the lake volume in equilibrium, mixes some input water of fixed chemistry and δD-δ18O composition to the residual water in the lake. Lerman (1979) suggested that the δD-δ18O steady-state of freezing lakes is reached after more than three residence times. Although the modeling reaches the same conclusion, the δD-δ18O composition of freezing lakes is not only determined by the residence time of water but also by the volume of ice that freezes annually which determines the volume of water that is added and mixes in the lake to maintain hydrological equilibrium. For mixing scenarios <~5%, the difference between δ18O input and equilibrium in the lake water approaches \( \ln(\alpha_{18O}) \); however, as the amount of annual mixing approaches 95%, the δ18O input and equilibrium approaches 0. In terms of deviation from the GMWL, the difference between D-excess of input and equilibrium in the lake water approaches 8% for annual mixing scenarios <5% and is reduced to near 0 as the amount of annual mixing approaches 95% (Figure 3D).

FREEZCH9 allows one to test for the effects of input water with differing isotopic signatures (i.e., evaporated water, meteoric water, cryo-freezing water) on the distribution of lake water isotopic composition in δD-δ18O space (Figure 7). Horita (2009) suggested that lakes with δD-δ18O composition plotting above...
the GMWL are reflective of being affected by the freezing process. The residual waters in well-sealed ice-covered lakes and subglacial lakes that are recharged by meteoric-like waters (i.e., plotting along the GMWL) should plot above the GMWL, regardless of their annual mixing rate. The extent to which the D-excess of these lakes will deviate from the GMWL will be a function of their annual mixing rate. This is the case for Lake Vostok (0.0037% annual mixing) where the δ18O of recharge water (−56.7‰) approximates that in the accreted ice (−56.2‰) and the water column is depleted by c. 3‰ (−59.0 ± 0.3‰) but with D-excess (17 ± 1‰) c. 10‰ higher than estimated for the input water (7.2‰).

In the case of well-sealed perennially ice-covered lakes or subglacial lakes recharged by surface or soil waters (e.g., ephemeral streams) and whose δD-δ18O composition is shifted below the GMWL due to evaporation, the δD-δ18O of the water column may not be shifted above the GMWL following the freezing process (Figure 7). The latter would be dependent on the extent of evaporation and mixing condition in the lake.

Finally, in the case of well-sealed perennially ice-covered lakes or subglacial lakes recharged by subglacial waters that have experienced freeze-concentration, the δD-δ18O of these lakes will strongly deviate above the GMWL for any mixing scenarios. That is because the recharge waters will have δD-δ18O composition plotting above the GMWL and the freezing process taking place in the lake will shift the δD-δ18O of the lake water further above the GMWL (but within the limits shown in Figures 3C,D). Such lakes may have D-excess that evolved to values greater than 17‰. It has been suggested that there might exist a regional groundwater system beneath the Antarctic Ice Sheet, as inferred for Lake Bonney in the McMurdo Dry Valleys from airborne transient electromagnetic sensor (i.e., Mikucki et al., 2015). If this regional groundwater system includes circulation through subglacial lakes, this isotopic signature could be used to infer the source of water (largely from basal melting or multiple freeze-concentration).

CONCLUSION

In this study, we developed an isotope-augmented version of FREEZCHEM (FREEZCH5) and made it recursive (FREEZCH9) to predict the δD-δ18O evolution and isotopic steady-state while accounting for changes in the ice-water isotope fractionation factor as freezing increases the salinity of the residual water. The following conclusions can be drawn from our results:

1. Unlike previous models, FREEZCH9 takes into consideration the combined effects of residual water mixing with incoming waters and evolving geochemistry on the stable water isotopic composition of well-sealed ice-covered lakes; it can be a tool to estimate the annual mixing fraction and residence time of the lake.

2. FREEZCH9 modeling of Lake Vostok suggests that the δD-δ18O composition of the upper water column should be −453.5 and −59.1‰, respectively; these are within error of the calculations of Ekaykin et al. (2016) (−455 ± 1‰ and −59.0 ± 0.3‰ for δD-δ18O, respectively).

3. FREEZCH9 modeling of Lake Untersee using 1% annual recharge and mixing with lake water suggests that the δ18O composition (−37.9 to −37.6‰) is in equilibrium with source waters having an average δ18O composition of −35.0‰. The lake is recharged from subaqueous melting of the Anuchin Glacier and subglacial meltwater. Based on the δ18O age-depth relation, the δ18O of the subaqueous melting of the Anuchin Glacier is estimated at −34.2‰ and two-component mixing indicates that the δ18O of subglacial meltwater is −35.8‰. The distribution of δD-δ18O of the oxic water above the AMWL with D-excess of 14‰ suggest that the lake has been well-sealed for the last 300–500 years and not been fed by surface waters (recharged only by subaqueous melting of the Anuchin Glacier and from subglacial meltwater).

4. The distribution of well-sealed ice-covered lakes in δD-δ18O space depends on the input water (i.e., evaporated water, meteoric water, cryo-freezing water) having different D-excess signatures. Hence, FREEZCH9 may be also used to determine if the hypothetical groundwater systems of the McMurdo Dry Valleys (i.e., Mikucki et al., 2015) are fully or partially recharged by subglacial lakes.

DATA AVAILABILITY STATEMENT

All datasets generated for this study are included in the article/Supplementary Material.

AUTHOR CONTRIBUTIONS

BF: manuscript writing (main contributor), data collection, data analysis and interpretation, and editing prior to manuscript’s submission. DL: manuscript writing, data collection, data interpretation, and editing prior to manuscript’s submission. DF: model development and editing prior to manuscript’s submission. KW and DA: data collection and editing prior to manuscript’s submission.

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SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/feart.2020.00220/full#supplementary-material

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Conflict of Interest: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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