TODIM Dynamic Emergency Decision-Making Method Based on Hybrid Weighted Distance Under Probabilistic Hesitant Fuzzy Information

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Abstract The classical TODIM method solves problems by expressing the attribute values as crisp numbers, thus incurring information loss. This paper, noting the ambiguity and fuzziness of information especially in a probabilistic hesitant fuzzy environment, develops a TODIM dynamic emergency decision-making method based on hybrid weighted distance. This method is suitable for emergency decision-making as it supports the rapidity and evolving nature of emergency responses, and accommodates the uncertainty of the external environment. A case study of a huge fire in China is used to validate the proposed method. The proposed TODIM method outperforms the methods proposed by Gao et al. in Int. J. Fuzzy. Syst. 19(5), 1261–1278 (2017) and Zhang et al. in Syst. 61, 48–58 (2014), suggesting its appeal in dealing with fuzzy information during emergency decision-making.

Keywords Probabilistic hesitant fuzzy set · TODIM · Hybrid weighted distance · Emergency decision-making · China

1 Introduction

Large-scale, high-risk but infrequent disasters at the provincial, national, and regional levels have wrought severe consequences to society [1, 2]. Some examples of such events include the Liangshan forest fire in Sichuan in 2019 resulting in the unnecessary deaths of 30 firefighters, the great Australian bushfire in 2020 in three Australian states, depleting 46 million acres of land, destroying 6000 farms, decimating half a billion native animals and unnecessary lives lost, and the COVID-19, which led to severe health and economic impacts globally with half a million fatalities. In all three disasters, emergency response decisions were needed at the national, regional, municipal, and firm levels. The decision-makers and stakeholders had to decide on the necessary courses of action and craft appropriate responses to bring the situation back to normalcy as quickly as possible, despite not fully knowing the extent of the collateral damage nor what will happen next in the emergency. Therefore, knowing how to make a decision quickly and accurately during an emergency response is now an agenda on many a decision-maker’s plates globally. The study of Emergency Decision-Making (EDM), and the establishment and improvement of an emergency response system are now a principal consideration when formulating national policy, especially in Asia. In the case of the public sector departments providing incomplete or inaccurate information, time urgency, and other uncontrollable externalities, EDM indeed has challenges on many fronts [3]. For instance, in China, natural
disasters are frequent, causing millions of deaths each year, leading to unnecessary economic loss, and hindering social development. Therefore, when a disaster occurs, the key question is to how to shorten the first response (i.e., EDM) and to select a reasonable emergency alternative to minimize the immediate losses [4–7]. In this regard, many studies have called for knowledge- and rule-based decision support systems. However, decision support systems often need to choose the best emergency plan based on many attributes. Therefore, EDM problems belong to the class of Multi-Attribute Decision-Making (MADM) problems [8]. Most works on EDM involve MADM, group decision-making (GDM), game theory, case reasoning technique, scenario construction, etc., as shown in Table 1.

Although the researches on emergency management are rich, they presupposes that the decision-maker (DM) is completely rational [17]. However, many studies have shown that DMs are bounded rational under the conditions of risk and uncertainty [9, 10, 18]. The DMs usually have a psychological expectation and are more sensitive to losses than gains [19]. With the irregularity in emergencies, the problem of emergency response veers more towards tackling the risks and uncertainties. Therefore, the psychological behavior of the DMs must be considered in the DM process. Most studies focused on prospect theory when considering the psychological behavior of the DMs [18]. However, a decision-making method based on prospect theory has an inherent limitation: the level of expectation needs to be known a priori, which is difficult to achieve.

Hence, this paper seeks to address this limitation by developing a distance measurement method based on the TODIM (an acronym in Portuguese of interactive and multiple attribute decision-making) method [20]. Compared with prospect theory, the advantage of the TODIM method is that the decision-making outcome is determined by computing the degree of gain or loss of an alternative relative to the rest, to better reflect the behavioral preference of the DMs such as reference dependence and loss aversion. At present, TODIM method has been extended to handle various types of fuzzy information, such as interval type-2 fuzzy information [21], triangular intuitionistic fuzzy numbers [22], Pythagorean uncertainty fuzzy linguistic information [23], interval numbers [24], probabilistic linguistic term sets [25] and so forth. It is undeniable that all hesitant fuzzy sets have their unique advantages. The reason why we choose probabilistic hesitant fuzzy sets is the evolution of emergency events, the change in the complex external environment, and other factors that have an impact on the EDM process. Therefore, we have to consider the probability of the change in the external environment. Probabilistic hesitant fuzzy sets accommodate more information uncertainty and reflect the preference of the DMs better.

Different from the other MADM problems such as supplier selection [26], EDM problems usually have high risk and uncertainty, and implementing the wrong EDM choice may lead to serious social consequences. Therefore, in the context of an emergency, DMs should avoid obtaining conflicting solutions and strive for higher-quality decision-making in the EDM process. Typically, the framework of the EDM process has two phases: an evaluation phase and a selection phase (see Fig. 1). In the evaluation phase, DMs provide their individual evaluation information based on their professional knowledge, experience, and similar historical emergency events. In the selection phase, an evaluation method is implemented to assess the alternatives and select the best course of action.

Although the researches on EDM have contributed to better emergency management [3, 9, 10], however, most of the related EDM methods assume that the decision-makers are psychological behavior independent and ignore the influence of the probability of occurrence in the external environment. Therefore, we develop a dynamic TODIM EDM method for emergencies in a probabilistic hesitant fuzzy environment, addressing two concerns:

1. Sometimes, the information to base the evaluation is supplied by a DM. Thus, noting the psychology of the DMs who provide the information can improve the decision-making outcomes. This is especially when the DMs operate in a complex and uncertain decision environment. So far, few studies apply the hybrid weighted distance using probabilistic hesitant fuzzy

### Table 1 Related studies on EDM

| Background | Methods | Literature |
|------------|---------|------------|
| Coal mine explosion | MADM | [3, 9, 10] |
| Barrier Lake Emergency | | |
| Explosions at Tianjin Port | GDM | [11, 12] |
| Selection of emergency shelter after earthquake | Scenario construction | [13] |
| Improving emergency response capability | Game theory | [14] |
| Settings for emergency exits | | |
| Man-made disaster situations post-disaster emergency resource planning | Case-based reasoning | [15, 16] |
information to handle emergencies considering the DM’s psychological behavior.  

2. Many researchers have tried to present different discussions about the EDM with hesitant fuzzy sets, albeit the management of other hesitant fuzzy sets in EDM has been done by using ranking models that present limitations. No study has used the TODIM method with an EDM approach based on a hybrid weighted distance under a probabilistic hesitant fuzzy environment. Thus, this paper will supply a realistic ranking method for a probabilistic hesitant fuzzy set that recognizes and facilitates the rapidly evolving EDM process.  

Furthermore, our proposed method can simulate an actual emergency environment, avoid information distortion or attenuation, provide policy support for the DMs, and provide robust solutions to complex large-scale emergencies, to minimize the loss of lives and livelihood.  

The rest of this paper is as follows: Sect. 2 presents some preliminaries. Section 3 develops a new probabilistic hesitant fuzzy hybrid weighted distance (PHFHWD) measure. Section 4 proposes a TODIM dynamic emergency decision-making method based on hybrid weighted distance under probabilistic hesitant fuzzy information. In Sect. 5, an example to evaluate the emergency response alternatives to the explosions at Tianjin Port is used to validate the proposed method. Section 6 concludes.

2 Preliminaries

This section introduces some preliminaries that will be used in the future sections, which include problem background, probabilistic hesitant fuzzy sets (PHFSs), and the classical TODIM method.  

2.1 Description of the Emergency Problem

When an emergency event occurs, it is usually dynamic and rapidly changing, fraught with much dissonance and uncertainty. At time $t_r$, the DMs can only obtain fuzzy information about the emergency from the first responders who sounded the alert. However, due to the sudden and urgent situation, the DMs can only make a preliminary assessment and act based on the history of similar emergencies, and personal experience. At time $t_{r+1}$, the emergency decision made at time $t_r$ would have been implemented in the interim. The DMs would need to decide on the measures to take in the next period based on the on-site information and the situation on the ground. For instance, unexpected strong winds may force an almost under control bush fire to change course and wreak havoc in a new locale, which may house more residents than expected. As such, the DMs have to modify the emergency response to obtain the best outcome. Hence, the DM, despite being affected by the change in external circumstance and already psychologically affected, has to decide when to re-select an emergency response. In short, the DMs have to dynamically adjust their decisions based on the latest available information to achieve the best emergency response outcome, as shown in Fig. 2.
2.2 Probabilistic Hesitant Fuzzy

Definition 1 [27] Let R be a fixed set, and then a PHFS $H_p$ on R is represented in the following mathematical symbol:

$$H_p = \{h(\gamma_i|p_i)|\gamma_i, p_i\},$$

where $h(\gamma_i|p_i)$ is a set of some probabilistic hesitant fuzzy elements (PHFEs) $\gamma_i|p_i$, $\gamma_i \in R$, $0 \leq \gamma_i \leq 1$, $i = 1, 2, \cdots, l_h$, and $l_h$ is the number of elements in $h(\gamma_i|p_i)$ (we denote it as $h(p)$ for short), $\gamma_i$ denotes the possible membership degrees of the element $x \in H_p$, and $p_i \in [0, 1]$ is the occurrence probability of $\gamma_i$, and $\sum_{i=1}^{l_h} p_i \leq 1$. If $\sum_{i=1}^{l_h} p_i < 1$, the PHFS is deemed incomplete. The complement of $h(\gamma_i|p_i)$ given by $h^C(\gamma_i|p_i) = \{((1 - \gamma_i)|p_i)|i = 1, 2, \cdots, l_h\}$.

Definition 2 [27] Let arbitrary $h(p) = \{\gamma_i|p_i|i = 1, 2, \cdots, l\}$ be the normalized PHFE, and $\bar{p}_i = p_i/\sum_{i=1}^{l_h} p_i$.

Definition 3 [28] For a PHFN $h(p) = \{\gamma_i|p_i|i = 1, 2, \cdots, l\}$, the score and deviation functions of $h(p)$ are defined, respectively, as

$$s(h(p)) = \sum_{i=1}^{l_h} \gamma_i \bar{p}_i,$$

$$v(h(p)) = \sum_{i=1}^{l_h} \bar{p}_i(s(h(p)) - \gamma_i)^2.$$

If $s(h_1(p)) > s(h_2(p))$, then $h_1(p) > h_2(p)$;

If $s(h_1(p)) < s(h_2(p))$, then $h_1(p) < h_2(p)$;

If $s(h_1(p)) = s(h_2(p))$, then

1. if $v(h_1(p)) > v(h_2(p))$, then $h_1(p) > h_2(p)$;
2. if $v(h_1(p)) < v(h_2(p))$, then $h_1(p) < h_2(p)$;
3. if $v(h_1(p)) = v(h_2(p))$, then $h_1(p) = h_2(p)$.

Definition 4 [29] Let $h_1(p)$ and $h_2(p)$ be two arbitrary PHFNs, then the probabilistic hesitant fuzzy Hamming distance between $h_1(p)$ and $h_2(p)$ is defined as:

$$d(h_1(p), h_2(p)) = \sum_{i=1}^{l_h} |\gamma_i^1 \bar{p}_i^1 - \gamma_i^2 \bar{p}_i^2|.$$

2.3 The Classical TODIM Method

To facilitate analysis and subsequent extensions, the classical TODIM method [20], which is on the base of prospect theory, is briefly introduced below.

Let $A = \{A_1, A_2, \cdots, A_n\}$ be a set of alternatives, where $A_i(i = 1, 2, \cdots, n)$ denotes $i$th alternative. Let $C = \{C_1, C_2, \cdots, C_m\}$ be a set of attributes, where $C_j(j = 1, 2, \cdots, m)$ denotes $j$th attribute. Let $\omega = (\omega_1, \omega_2, \cdots, \omega_m)^T$ be a vector of attribute weights, where $\omega_j(\omega_j \in [0, 1], \sum_{j=1}^{m} \omega_j = 1)$ denotes the weight of attribute $C_j$. The algorithmic for the classic TODIM method is as follows:

Step 2.3.1: Form the decision matrix $X = [x_{ij}]_{n \times m}$ comprising $n$ alternatives and $m$ evaluation attributes.

Step 2.3.2: Normalize the decision matrix $X = [x_{ij}]_{n \times m}$ into $X = [\bar{x}_{ij}]_{n \times m}$, according to the cost and benefits attribute. This renders the decision matrix dimensionless and the matrix elements comparable.

Step 2.3.3: Calculate the relative weight $\omega_r = \omega_j/\omega_r$, where $\omega_r = \max\{\omega_j, j = 1, 2, \cdots, n\}$.

Step 2.3.4: The dominance degree $\phi_i(A_i, A_q)$ of alternative $A_i$ over alternative $A_q$ for the attribute $C_j$ is calculated.
where \( \theta \) is the attenuation coefficient of the losses. If \( d_{ij} - d_{ij} > 0(\text{or} d_{ij} < 0) \), then \( d_{ij} - d_{ij} \) represents the gain (loss) of alternative \( A_i \) over alternative \( A_q \) for the attribute.

**Step 2.3.5:** The comprehensive dominance degree \( \phi(A_i;A_q) \) of alternative \( A_i \) over the alternative \( A_q \) is found from

\[
\phi(A_i;A_q) = \sum_{j=1}^{m} \phi_j(A_i;A_q), \quad i, q = 1, \ldots, n. \tag{6}
\]

**Step 2.3.6:** The overall dominance value \( \Phi(A_i) \) of alternative \( A_i \) is obtained according to

\[
\Phi(A_i) = \frac{\sum_{q=1}^{n} \phi(A_i;A_q) - \min \sum_{q=1}^{n} \phi(A_i;A_q)}{\max \sum_{q=1}^{n} \phi(A_i;A_q) - \min \sum_{q=1}^{n} \phi(A_i;A_q)}. \tag{7}
\]

**Step 2.3.7:** The alternatives are then ranked in descending order, based on their scores. We choose the highest (i.e., maximum dominance score) as the best choice.

### 3 Probabilistic Hesitant Fuzzy Hybrid Weighted Distance

**Definition 5** Let \( H_{p1} = \{h(\gamma_i|p_i)|\gamma_i, p_i\} \) and \( H_{p2} = \{h(\gamma_i|p_i)|\gamma_i, p_i\} \) are two PHFSs, then the probabilistic hesitant fuzzy weighted distance (PHFWD) between \( H_{p1} \) and \( H_{p2} \) is given by:

\[
\text{PHFWD}(H_{p1}, H_{p2}) = \left( \sum_{j=1}^{m} \omega_j \left( \text{d}_p(h(\gamma_i|p_i), h(\gamma_i|p_i)) \right)^{\frac{1}{2}} \right)^{\frac{1}{2}}, \tag{8}
\]

where \( \omega_j (j = 1, 2, \ldots, m)^T \) is a weight vector, with \( \omega_j \in [0, 1], \sum_{j=1}^{m} \omega_j = 1 \). Sometimes, the number of elements in \( H_{p1} \) is not equal to the number of elements in \( H_{p2} \), i.e., \( l_{H_{p1}} \neq l_{H_{p2}} \). In this paper, the risk attitude of the DMs is used to determine which added element will make the length of two PHFE’s equal. For this, we set \( h_i^+ = \max \{\gamma, p_i\} \) and \( h_i^- = \min \{\gamma, p_i\} \). If the DM is risk neutral, the added element is \( h = 0.5 \times (h_i^+ + h_i^-) \). If the DM is risk averse (seeker), the added element is \( h = h_i^+ (h = h_i^-) \).

Furthermore, when \( \lambda = 1 \), the PHFWD measure is reduced to the probabilistic hesitant fuzzy weighted Hamming distance (PHFWDH) measure. When \( \lambda = 2 \), then the PHFWD measure is reduced to the probabilistic hesitant fuzzy weighted Euclidean distance (PHFWEWD) measure. The PHFWD measure only considers the importance of the PHFEs, but not the importance of their position.

**Definition 6** Let \( H_{p1} = \{h(\gamma_i|p_i)|\gamma_i, p_i\} \) and \( H_{p2} = \{h(\gamma_i|p_i)|\gamma_i, p_i\} \) are two PHFSs, and the probabilistic hesitant fuzzy ordered weighted distance (PHFOWD) between \( H_{p1} \) and \( H_{p2} \) has the following form:

\[
\text{PHFOWD}(H_{p1}, H_{p2}) = \left( \sum_{j=1}^{m} w_j \left( H(\gamma_i, p_i) \right)^{\frac{1}{2}} \right)^{\frac{1}{2}}, \tag{9}
\]

where \( w_j (j = 1, 2, \ldots, m)^T \) is an order weight vector, with \( w_j \in [0, 1], \sum_{j=1}^{m} w_j = 1 \). “(\sigma(1), \sigma(2), \ldots, \sigma(j))” is the order of “(1, 2, \ldots, j)”, such as \( \sigma(j) \) is the \( j \)th largest PHFE among the PHFS. In particular, when \( \lambda = 1 \), then the PHFOWD measure is reduced to the probabilistic hesitant fuzzy ordered weighted Hamming distance (PHFOWHD) measure; when \( \lambda = 2 \), then the PHFOWD measure is reduced to the probabilistic hesitant fuzzy ordered weighted Euclidean distance (PHFOWED) measure.

Clearly, from definitions 5 and 6, the weight of the PHFWD measure stresses on the importance of the evaluation attribute while the weight of the PHFOWD measure stresses on the importance of the position of the attribute. However, both distance measures (i.e., PHFWD and PHFOWD) can only consider a single aspect of weight, but not both. Therefore, we propose a probabilistic hesitant fuzzy hybrid weighted distance (PHFHWHD) measure.

**Definition 7** Let \( H_{p1} = \{h(\gamma_i|p_i)|\gamma_i, p_i\} \) and \( H_{p2} = \{h(\gamma_i|p_i)|\gamma_i, p_i\} \) be two PHFSs, and the probabilistic hesitant fuzzy hybrid weighted distance (PHFHWHD) between \( H_{p1} \) and \( H_{p2} \) is given by:

\[
\text{PHFHWHD}(H_{p1}, H_{p2}) = \left( \sum_{j=1}^{m} w_j \left( \text{d}_p(h(\gamma_i, p_i), h(\gamma_i, p_i)) \right)^{\frac{1}{2}} \right)^{\frac{1}{2}}, \tag{10}
\]

where \( \text{d}_p(h(\gamma_i, p_i), h(\gamma_i, p_i)) \) is the \( j \)th largest element among \( \text{d}_p(h(\gamma_i, p_i), h(\gamma_i, p_i)), \text{d}_p(h(\gamma_i, p_i), h(\gamma_i, p_i)) = \)
Similarly, when \( \lambda = 1 \), the PHFOWD measure is reduced to the probabilistic hesitant fuzzy hybrid weighted Hamming distance (PHFHWD) measure; when \( \lambda = 2 \), then the PHFWD measure is reduced to the probabilistic hesitant fuzzy hybrid weighted Euclidean distance (PHFHWD) measure.

Theorem 1 PHFWD and PHFOWD measures are special cases of PHFHWD measure.

Proof Set \( w = \left( \frac{1}{n}, \ldots, \frac{1}{n} \right)^T \) and \( \lambda = 1 \), then

\[
\text{PHFHWD}(H_{p1}, H_{p2}) = \left( \frac{1}{n} \sum_{j=1}^{n} \left( \sum_{j=1}^{m} w_j d(p_h, (\gamma_i, p_i)) \right)^{\frac{1}{2}} \right) \\
= \left( \frac{1}{n} \sum_{j=1}^{m} \left( \sum_{j=1}^{n} \frac{1}{n} \text{PHFWD}(h_1(\gamma_i, p_i), h_2(\gamma_i, p_i)) \right)^{\frac{1}{2}} \right) \\
= \text{PHFWD}(H_{p1}, H_{p2}).
\]

Furthermore, \( \omega = \left( \frac{1}{n}, \ldots, \frac{1}{n} \right)^T \), then

\[
\text{PHFHWD}(H_{p1}, H_{p2}) = \left( \frac{1}{n} \sum_{j=1}^{n} \left( \sum_{j=1}^{m} w_j d(p_h, (\gamma_i, p_i)) \right)^{\frac{1}{2}} \right) \\
= \left( \frac{1}{n} \sum_{j=1}^{m} \left( \sum_{j=1}^{n} \frac{1}{n} \text{PHFWD}(h_1(\gamma_i, p_i), h_2(\gamma_i, p_i)) \right)^{\frac{1}{2}} \right) \\
= \text{PHFOWD}(H_{p1}, H_{p2}).
\]
Before handling emergency incidents, we check the relevant records to sight similar past emergencies. If such records exist, we refer to how such emergencies were handled, to deal with the current situation. Otherwise, the DMs should discuss and craft a response. Next, we kick start the emergency response procedure. The evaluation value of an emergency can vary with time, depending on the severity of the situation. To make a dynamic decision based on the evaluation value given by the DMs at different instances, we call on the following steps:

Step 1: The DMs evaluate alternative \( A_i \) on attribute \( C_j \), given that emergency state \( Z_t (t = 1) \) occurs. The evaluation results are expressed by PHFE \( h_{ij}^T (\gamma_i \mid p_i) \), and then the decision matrix \( D_s = (h_{ij}^T (\gamma_i \mid p_i))_{m \times n} \) is obtained.

Step 2: Normalize \( D_s = (h_{ij}^T (\gamma_i \mid p_i))_{m \times n} \) into matrix \( h_{ij}^K = (h_{ij}^T (\gamma_i \mid p_i))_{m \times n} \). An attribute is either cost or benefit attribute. Suppose the normalized attribute value is \( h_{ij}^T (\gamma_i \mid p_i) \), then the normalized attribute value is \( h_{ij}^K (\gamma_i \mid p_i) = h_{ij}^T (\gamma_i \mid p_i) \), the normalized cost attribute is \( h_{ij}^C (\gamma_i \mid p_i) = h_{ij}^T ((1 - \gamma_i) \mid p_i) \), respectively.

Step 3: Aggregate the normalized attribute value using Eq. (11):

\[
\begin{align*}
PHFWA & (h_{ij}^T (\gamma_i \mid p_i), h_{ij}^T (\gamma_i \mid p_i), \ldots, h_{ij}^T (\gamma_i \mid p_i)) \\
&= \bigoplus_{k=1}^{s} (o_{k} \delta_{ij}^T (\gamma_i \mid p_i)) \\
&= \sum_{k=1}^{s} \{1 - \prod_{k=1}^{n} \left[ \frac{1 - \gamma_{ij}^{k}}{\gamma_{ij}^{k}} \right] \}.
\end{align*}
\]

Step 4: Find the weight of attributes. In this paper, the score function and the entropy weight method [30] are combined to find the weight of attributes:

\[
b_{ij} = \frac{s_{ij} (h(p))}{\sum_{j=1}^{n} s_{ij} (h(p))},
\]

\[
E_j = -\sigma \sum_{i=1}^{n} b_{ij} \ln b_{ij},
\]

\[
o_j = \frac{(1 - E_j)}{\sum_{j=1}^{n} (1 - E_j)},
\]

where \( \sigma = \frac{1}{\ln n} \), \( 0 \leq E_j \leq 1 \).

Step 5: Obtain PHFHWD (\( H_{pi}, H_{pi} \)) and PHFHWD (\( H_{pi}, H_{pi} \)) measures using Eq. (10), where \( H_{pi} \) and \( H_{pi} \) are the probabilistic hesitant fuzzy positive ideal solution (PHFPIS) and probabilistic hesitant fuzzy negative ideal solution (PHFNIS), respectively.

Step 6: Find dominance degree \( \phi_j (A_i, A_q) \) of alternative \( A_i \) over alternative \( A_q \) for attribute \( C_j \) using Eq. (5).
The DMs proposed five attributes for the emergency rescue work after observing analyzing the fire situation on the scene, combining with similar historical cases, their professional knowledge and referring to the “Code for Classification and Coding of Emergency Events”:

\( C_1 \): Possibility of more explosions during the rescue (due to the flammability of the goods)

\( C_2 \): Weather conditions at the time of rescue (presence of strong winds)

\( C_3 \): Ease of rescue (any blockages to the warehouse)

\( C_4 \): Timeliness of rescue (before the heat becomes too strong for rescue work)

\( C_5 \): Cost of rescue (potential lives lost).

From the analysis of the experts, the rescue and chemicals disposal team, and the weather reports, the port may encounter three situations or states in the next 72 h:

\( Z_1 \): in the \( t_1 \) stage, the weather becomes cloudy and the light southwest breeze will blow the gaseous emissions from the dangerous goods towards the Bohai Sea. With a sea breeze, the fire may intensify, widening the area of the blaze. As the specific explosive is unknown, a high probability of re-explosion in the stage cannot be discounted.

\( Z_2 \): in the \( t_2 \) stage, a thunderstorm may occur and a strong southwest wind will blow the gaseous emissions from the dangerous goods towards the Bohai Sea. While a thunderstorm may dampen the fire, the DMs are not certain if the thunderstorm can quench the fire. However, because cyanide is a water-soluble toxic substance, it will be affected by a thunderstorm. There is also the concern of Cyanide dissolved in water leaking into the city.

\( Z_3 \): in the \( t_3 \) stage, the weather is clear, the southwest breeze will disperse the gaseous emissions from the dangerous goods towards the Bohai Sea, which is helpful for the diffusion of the contaminant in the air. Depending on the success of the previous fire-fighting work, the fire may be under control. Suppose the specific explosives are identified. It is necessary to enter the explosion site with biochemical troops for search and rescue and hazardous chemical cleaning.

### 5.1 Decision Steps

**Step 1:** The DMs evaluate alternative \( A_i \) given that a certain state \( Z_t \) has occurred concerning attribute \( C_j \) and the data

| DM | Alternative | Attribute |
|----|-------------|-----------|
| \( e_1 \) | \( A_1 \) | (0.841.0) (0.661.0) (0.6510.4, 0.8610.2) (0.6910.5) (0.6910.4, 0.7910.4) |
|      | \( A_2 \) | (0.8610.4, 0.7910.5) (0.7610.4, 0.7910.5) (0.7610.4) (0.8110.4, 0.8210.3) (0.8110.4) |
|      | \( A_3 \) | (0.8910.5, 0.7910.3) (0.8211.0) (0.7610.0) (0.8910.5, 0.7910.3, 0.6710.2) |
| \( e_2 \) | \( A_1 \) | (0.7311.0) (0.8210.4, 0.7210.6) (0.6510.4, 0.8610.4, 0.9610.2) (0.8011.0) (0.8210.6, 0.7610.4) |
|      | \( A_2 \) | (0.7610.4, 0.6910.5, 0.8610.1) (0.7610.4, 0.6910.5) (0.8610.4, 0.7910.5) (0.7610.1) (0.8110.4) |
|      | \( A_3 \) | (0.6910.4, 0.5910.6) (0.7610.4, 0.6910.5, 0.8610.1) (0.6810.3, 0.7310.5) (0.6810.2) (0.6210.0) |
| \( e_3 \) | \( A_1 \) | (0.4911.0) (0.5210.4, 0.6210.6) (0.7810.6, 0.8910.4) (0.6910.3, 0.7610.5, 0.8810.2) (0.8710.3, 0.6710.6, 0.9310.2) |
|      | \( A_2 \) | (0.6910.6, 0.5910.4) (0.6511.0) (0.8910.6, 0.9210.3) (0.7910.3, 0.6810.5) (0.8210.3, 0.7310.6, 0.6310.1) |
|      | \( A_3 \) | (0.6310.3, 0.6610.4) (0.6310.3, 0.7310.4, 0.6910.3) (0.7910.6, 0.7110.4) (0.8710.7, 0.7110.3) (0.8210.4, 0.7210.6) |
| \( e_4 \) | \( A_1 \) | (0.6310.2, 0.7310.6, 0.8910.2) (0.5510.6, 0.6110.4) (0.6010.8, 0.7010.2) (0.3310.4, 0.4510.6) (0.6310.3, 0.7310.3, 0.8910.4) |
|      | \( A_2 \) | (0.5310.5, 0.6510.5) (0.4010.3, 0.5510.3, 0.6910.4) (0.5010.2, 0.6010.3, 0.7101.5) (0.6010.6, 0.7510.2) (0.7010.5, 0.8010.5) |
|      | \( A_3 \) | (0.8010.5, 0.8510.3, 0.9010.2) (0.3510.2, 0.4410.4, 0.5010.4) (0.5610.2, 0.6610.8) (0.5010.4, 0.6510.6) (0.6210.3, 0.7510.7) |
for analysis are expressed by PHFHE $h^{ij}_{k'}(y_{i}|p_{j})$. The decision matrix $D' = (h^{ij}_{k'}(y_{i}|p_{j}))_{m \times n}$ is obtained. The results are shown in Tables 2, 3, 4.

Step 2: Because attribute $C_1$ and attribute $C_3$ belong to cost attribute, attribute $C_2$, attribute $C_4$, and attribute $C_5$ belong to benefit attribute. Therefore, the normalized decision matrices are shown in Tables 5, 6, 7.

Step 3: Aggregate the normalized attribute value using Eq. (11), the result can be seen in Table 8.

Step 4: According to Eqs. (12, 13, 14), the attribute weight in different states can be obtained as follows:

In $Z_1$ state, the attribute weights are $\omega_{Z1} = (0.322, 0.059, 0.187, 0.075, 0.358)^T$;

In $Z_2$ state, the attribute weights are $\omega_{Z2} = (0.204, 0.112, 0.039, 0.297, 0.347)^T$;

In $Z_3$ state, the attribute weights are $\omega_{Z3} = (0.394, 0.192, 0.045, 0.066, 0.303)^T$.

Step 5: Calculate PHFHWDM ($H_{p1}$, $H_{p+}$) and PHFHWDM ($H_{p2}$, $H_{p-}$) measures using Eq. (10), where $H_{p+}$ and $H_{p-}$ are denoted as probabilistic hesitant fuzzy positive ideal solution (PHFPIS) and probabilistic hesitant fuzzy negative ideal solution (PHFNIS), respectively. Assume that the ordered weights are $w = (0.26, 0.35, 0.39)^T$, according to the score function, the PHFPIS and PHFNIS in different states can be obtained as follows:

\[
H_{p+}^{Z1} = \{(0.30|0.36, 0.33|0.56, 0.29|0.08),
(0.68|0.21, 0.70|0.69, 0.76|0.10),
(0.79|0.23, 0.78|0.42, 0.82|0.35),
(0.78|0.46, 0.77|0.42, 0.69|0.12),
(0.29|0.13, 0.28|0.44, 0.28|0.44)\}
\]

\[
H_{p-}^{Z2} = \{(0.38|0.42, 0.36|0.47, 0.47|0.31),
(0.71|0.32, 0.71|0.61, 0.74|0.07),
(0.66|0.05, 0.74|0.25, 0.78|0.70),
(0.74|0.32, 0.77|0.48, 0.72|0.20),
(0.39|0.58, 0.36|0.17, 0.21|0.25)\}
\]

\[\text{Table 3 Evaluation values of alternative in state } Z_2\]

| DM | Alternative | Attribute | $C_1$ | $C_2$ | $C_3$ | $C_4$ | $C_5$ |
|----|-------------|-----------|------|------|------|------|------|
| $e_1$ | $A_1$ | (0.800.5, 0.850.3, 0.890.2) | (0.780.6, 0.820.2) | (0.680.4, 0.750.3, 0.890.3) | (0.500.5, 0.670.5) | (0.730.4, 0.870.3) |
|   | $A_2$ | (0.680.5, 0.7210.5) | (0.530.5, 0.670.5) | (0.760.3, 0.870.7) | (0.500.3, 0.600.3, 0.700.4) | (0.700.2, 0.800.2, 0.900.4) |
|   | $A_3$ | (0.760.4, 0.790.5) | (0.690.3, 0.760.6, 0.880.2) | (0.651.0) | (0.801.0) | (0.820.6, 0.760.4) |
| $e_2$ | $A_1$ | (0.760.4, 0.690.5, 0.860.1) | (0.760.4, 0.690.5) | (0.860.4, 0.790.5) | (0.761.0) | (0.810.4) |
|   | $A_2$ | (0.530.5, 0.7710.5) | (0.720.7, 0.800.2, 0.900.1) | (0.530.2, 0.600.3, 0.740.5) | (0.630.6, 0.710.2) | (0.550.7, 0.600.2, 0.840.1) |
|   | $A_3$ | (0.510.4, 0.630.6) | (0.630.7, 0.700.3) | (0.600.3, 0.700.4, 0.840.3) | (0.630.5, 0.700.5) | (0.500.7, 0.600.2, 0.840.1) |
| $e_3$ | $A_1$ | (0.491.0) | (0.520.4, 0.620.6) | (0.780.6, 0.890.4) | (0.690.3, 0.760.5, 0.880.2) | (0.870.3, 0.670.6, 0.930.2) |
|   | $A_2$ | (0.530.5, 0.650.5) | (0.400.3, 0.550.3, 0.690.4) | (0.500.2, 0.600.3, 0.710.5) | (0.600.6, 0.750.2) | (0.700.5, 0.800.5) |
|   | $A_3$ | (0.630.3, 0.660.4) | (0.630.3, 0.730.4, 0.690.3) | (0.790.6, 0.710.4) | (0.870.7, 0.710.3) | (0.820.4, 0.720.6) |
| $e_4$ | $A_1$ | (0.500.2, 0.600.3, 0.700.5) | (0.720.6, 0.800.2) | (0.300.4, 0.500.6) | (0.650.5, 0.700.2, 0.830.3) | (0.600.5, 0.700.5) |
|   | $A_2$ | (0.710.4, 0.830.4) | (0.650.5, 0.700.1, 0.830.4) | (0.771.0) | (0.530.5, 0.670.5) | (0.510.4, 0.630.6) |
|   | $A_3$ | (0.800.5, 0.850.3, 0.90.2) | (0.350.2, 0.440.4, 0.500.4) | (0.560.2, 0.660.8) | (0.500.4, 0.650.6) | (0.620.3, 0.750.7) |
Table 4 Evaluation values of alternative in state $Z_3$

| DM  | Alternative | Attribute | $C_1$       | $C_2$       | $C_3$       | $C_4$       | $C_5$       |
|-----|-------------|-----------|-------------|-------------|-------------|-------------|-------------|
| $e_1$ | $A_1$       | (0.550.2, 0.630.6, 0.790.2) | (0.520.4, 0.610.6) | (0.510.4, 0.630.6) | (0.510.4, 0.630.6) | (0.710.4, 0.830.1, 0.950.5) | |
|      |             |           | (0.670.5, 0.850.5) | (0.400.3, 0.550.3, 0.690.4) | (0.500.2, 0.600.3, 0.710.5) | (0.600.6, 0.750.2) | (0.700.5, 0.800.5) |
|      | $A_2$       | (0.800.5, 0.850.3, 0.90.2) | (0.650.5, 0.700.2, 0.830.3) | (0.510.4, 0.630.6) | (0.500.4, 0.650.6) | (0.620.3, 0.750.7) | |
|      | $A_3$       | (0.791.0) | (0.300.4, 0.500.6) | (0.580.3, 0.790.7) | (0.590.5, 0.660.3, 0.810.2) | (0.870.3, 0.670.6, 0.930.2) | |
| $e_2$ | $A_1$       | (0.630.6, 0.560.4) | (0.651.0) | (0.890.6, 0.920.3) | (0.790.3, 0.680.5) | (0.820.3, 0.730.6, 0.630.1) | |
|      |             |           | (0.430.3, 0.660.4) | (0.630.3, 0.730.4, 0.690.3) | (0.790.6, 0.710.4) | (0.870.6, 0.710.4) | (0.820.4, 0.720.6) |
|      | $A_2$       | (0.881.0) | (0.661.0) | (0.870.7, 0.710.3) | (0.690.5) | (0.690.6, 0.740.4) | |
|      | $A_3$       | (0.710.4, 0.890.5) | (0.890.6, 0.920.3) | (0.760.8) | (0.810.4, 0.820.3) | (0.810.4) | |
| $e_3$ | $A_1$       | (0.890.5, 0.790.3) | (0.821.0) | (0.761.0) | (0.860.6, 0.790.3, 0.570.1) | (0.801.0) | |
|      |             |           | (0.731.0) | (0.790.3, 0.680.5) | (0.670.4, 0.830.3, 0.960.3) | (0.801.0) | (0.820.6, 0.760.4) |
|      | $A_2$       | (0.760.5, 0.690.2, 0.860.3) | (0.630.6, 0.560.4) | (0.860.4, 0.790.5) | (0.861.0) | (0.710.8) | |
|      | $A_3$       | (0.690.4, 0.590.6) | (0.760.4, 0.690.5, 0.860.1) | (0.570.3, 0.760.5, 0.660.5, 0.730.5) | (0.621.0) | | |

PHFHWD is calculated under different states and different $i$, and the results can be seen in Table 9.

**Step 6:** The results from step 5 are put into Eq. (5), yielding the dominance degree $\phi_j(A_i, A_{+})$ and $\phi_j(A_i, A_{-})$ of alternative $A_i$ over PHFPIs $A_+$ and PHFNIS $A_-$, respectively. Table 10 shows the results.

**Step 7:** Calculate comprehensive dominance degree $\phi(A_i, A_q)$ of alternative $A_i$ over alternative $A_q$ for attribute $C_j$ using Eq. (6). The results can be seen in Table 11.

**Step 8:** Find the overall dominance value $\Phi(A_i)$ of alternative $A_i$, and rank the alternatives using $\Phi(A_i)$. The larger $\Phi(A_i)$ is, the better is alternative $A_i$ as an emergency response (Table 12).

**Step 9:** From Table 12, the ranking obtained by the proposed method is insensitive to $\lambda$. The optimal emergency response changes with state $Z_i$, which also explains the need to consider the EDM method from a dynamic perspective. The best emergency response for each state is now provided as a tuple: $(Z_1, A_2), (Z_2, A_3), (Z_3, A_3)$. Next, Fig. 4 shows the effect of a change in the parameter $\lambda$ on the overall dominance value. Notably, as $\lambda$ changes for each $Z_i$, and altering the overall dominance
value of the alternatives, the ranking outcomes remain unchanged.

5.2 Comparative Analysis

To highlight the effectiveness and practicability of the proposed method, we perform comparative analysis for the proposed method from two aspects:

(1) The method proposed in this paper is compared with the probabilistic hesitant fuzzy distance measure proposed by Gao et al. [29], which ignored the psychological behavior of the decision-makers.

(2) The method proposed in this paper is compared with the TODIM analysis approach under a hesitant fuzzy environment [31], which considered the psychological behavior of decision-makers but ignored the occurring probabilities of the changes of external environment.

5.2.1 Comparison with the Probabilistic Hesitant Fuzzy Distance Measure

Tables 13 and 14 show the comparison results of the ranking with the probabilistic hesitant fuzzy distance measure [29].

Tables 13 and 14 show that both methods yield different results for the same state and $\lambda$. The results obtained from the proposed method are more stable for different values of $\lambda$ than those obtained from [29]. The decision outcomes are different under the two methods for the same fuzzy decision-making environment because some information was lost in [29]. This suggests that DM’s psychological behavior can influence the decisions made. Hence, embedding the psychological behavior of the DMs can pan out a more realistic selection outcome.

5.2.2 Comparison with the TODIM Analysis Approach Under a Hesitant Fuzzy Environment

Similarly, we compare our results against the TODIM analysis method under a hesitant fuzzy environment [31], which is used to handle the same emergency event employed in this paper, but without considering the
possibility of the alteration of the external environment. To do this, we remove the probabilities, i.e., the probabilistic hesitant fuzzy numbers in Tables 2, 3, and 4 are now hesitant fuzzy numbers. Applying the TODIM approach under a hesitant fuzzy environment in [31] yields the required ranking results (see Tables 15, 16).

Tables 15 and 16 show that by applying [31], the best choice is state-dependent for the same $k$ and $k$ is dependent for the same state. Hence, there would be difficulty in reaching a consensus-based best emergency response. The former is easy to be understood since the best choice for each state need not necessarily be the same. $k$ is not a factor that affects the DM’s psychological behavior, the latter case would suggest that we need to factor the DM’s psychology. The proposed method presents more robust decision responses, as shown in state $Z_1$, where the optimal response under a hesitant fuzzy environment is such that $A_3 \rightarrow A_2$ when $\lambda$ shifts. The results under a probabilistic hesitant fuzzy environment hold at $A_2 \rightarrow A_2$, when $\lambda$ shifts. The reason is that the occurrence probabilities of the change in the emergency are downplayed.

### 5.3 Discussion

From the comparisons conducted, some advantages of the proposed method are summarized as:

1. Our method treats not only the importance of the attribute, but also the importance of the position of the attribute. As such, we can improve the TODIM method through our approach to take into account the psychological behavior of the DMs by appropriately recognizing such positions.

2. Compared to Zhang et al. [31], our approach acknowledges the rapidity of the external environment and weights it accordingly by assigning a
position of importance to the attribute weights to reflect the preference of the DMs, thus avoiding the loss of pertinent information. The proposed method recognizes both the dynamism of emergency decision-making situations and the mental pressures faced by the DMs, akin to an actual large-scale emergency decision-making environment. This method serves better in practical emergency response situations. The proposal provides theoretical support for practical application and at the same time provides a reference for the policy formulation of emergency departments. However, the method proposed in this paper has a limitation, that is, the mathematical model of probabilistic hesitant fuzzy numbers cannot be universally applied to other types of fuzzy decision-making problems.

6 Conclusion and Future Works

With uncertainty in the external environment, the vagueness and complexity of emergencies may exert more challenges for decision-makers. The probabilistic hesitant fuzzy set is the latest extension of the hesitant fuzzy set, which is intended to cope with changes in the external environment. We extend this approach by considering simultaneously the changes in the importance of the criteria and importance of the position of that criteria, particularly where it concerns the psychology of the decision-makers and the dynamic external environment. Specifically, we introduce the concept of the hybrid weighted distance of the probabilistic hesitant fuzzy set to extend the TODIM method to increase the flexibility and richness of dealing with dynamic EDM problems. In short, this paper dynamically adjusts the emergency response according to
Table 8 Group decision-making matrix for the three states

| State | Alternative | Attribute |
|-------|-------------|-----------|
| \( Z_1 \) | \( A_1 \) | (0.340.20, 0.320.60, 0.280.20) |
| | \( A_2 \) | (0.300.36, 0.330.56, 0.290.08) |
| | \( A_3 \) | (0.250.45, 0.280.33, 0.270.22) |
| \( Z_2 \) | \( A_1 \) | (0.380.42, 0.360.47, 0.310.11) |
| | \( A_2 \) | (0.390.33, 0.390.33, 0.260.33) |
| | \( A_3 \) | (0.340.33, 0.310.33, 0.260.33) |
| \( Z_3 \) | \( A_1 \) | (0.270.20, 0.250.60, 0.200.20) |
| | \( A_2 \) | (0.310.53, 0.330.21, 0.220.26) |
| | \( A_3 \) | (0.320.50, 0.360.27, 0.270.24) |

Table 9 PHFHWD measure for \( Z_i \) and different \( \lambda \)

| State | \( \lambda \) | \( \text{PHFHWD}(H_{i_1}, H_{i_2}) \) | \( \text{PHFHWD}(H_{i_1}, H_{i_3}) \) |
|-------|-------------|-----------------|-----------------|
| \( Z_1 \) | \( \lambda = 1 \) | \( A_1 \) | 0.002 | 0.010 | 0.002 | 0.014 | 0.004 | 0.032 | 0.019 | 0.005 | 0.000 | 0.000 |
| | | \( A_2 \) | 0.000 | 0.000 | 0.001 | 0.001 | 0.003 | 0.027 | 0.018 | 0.001 | 0.000 | 0.000 |
| | | \( A_3 \) | 0.000 | 0.000 | 0.000 | 0.011 | 0.004 | 0.024 | 0.003 | 0.001 | 0.000 | 0.000 |
| | \( \lambda = 2 \) | \( A_1 \) | 0.042 | 0.011 | 0.072 | 0.014 | 0.041 | 0.124 | 0.067 | 0.019 | 0.000 | 0.000 |
| | | \( A_2 \) | 0.000 | 0.000 | 0.009 | 0.045 | 0.008 | 0.107 | 0.064 | 0.006 | 0.028 | 0.018 |
| | | \( A_3 \) | 0.000 | 0.000 | 0.000 | 0.049 | 0.041 | 0.022 | 0.011 | 0.052 | 0.000 | 0.000 |
| \( Z_2 \) | \( \lambda = 1 \) | \( A_1 \) | 0.000 | 0.000 | 0.001 | 0.015 | 0.009 | 0.016 | 0.024 | 0.007 | 0.000 | 0.000 |
| | | \( A_2 \) | 0.000 | 0.000 | 0.005 | 0.014 | 0.002 | 0.063 | 0.001 | 0.002 | 0.000 | 0.000 |
| | | \( A_3 \) | 0.000 | 0.010 | 0.001 | 0.002 | 0.002 | 0.020 | 0.035 | 0.018 | 0.000 | 0.000 |
| | \( \lambda = 2 \) | \( A_1 \) | 0.000 | 0.000 | 0.011 | 0.071 | 0.068 | 0.078 | 0.089 | 0.035 | 0.004 | 0.000 |
| | | \( A_2 \) | 0.000 | 0.000 | 0.025 | 0.064 | 0.030 | 0.180 | 0.012 | 0.010 | 0.000 | 0.000 |
| | | \( A_3 \) | 0.000 | 0.033 | 0.035 | 0.17 | 0.005 | 0.102 | 0.119 | 0.074 | 0.000 | 0.000 |
| \( Z_3 \) | \( \lambda = 1 \) | \( A_1 \) | 0.001 | 0.001 | 0.021 | 0.021 | 0.005 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| | | \( A_2 \) | 0.000 | 0.000 | 0.006 | 0.006 | 0.004 | 0.056 | 0.017 | 0.013 | 0.001 | 0.000 |
| | | \( A_3 \) | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.034 | 0.035 | 0.021 | 0.001 | 0.000 |
| | \( \lambda = 2 \) | \( A_1 \) | 0.007 | 0.010 | 0.101 | 0.075 | 0.050 | 0.003 | 0.000 | 0.000 | 0.000 | 0.000 |
| | | \( A_2 \) | 0.000 | 0.000 | 0.020 | 0.034 | 0.031 | 0.092 | 0.128 | 0.055 | 0.005 | 0.005 |
| | | \( A_3 \) | 0.000 | 0.000 | 0.000 | 0.005 | 0.006 | 0.133 | 0.097 | 0.101 | 0.010 | 0.000 |
the development of the emergency, recognizing the fluidity of such events. At the end, the novelty of this paper has been demonstrated by the background of the Tianjin Port fire and explosion accident. This paper, therefore, contributes to probabilistic hesitant fuzzy set EDM research in attempting to model the dynamics and uncertainty of the external environment. However, the proposed method has a limitation, that is, the mathematical model of probabilistic hesitant fuzzy numbers cannot yet be universally applied to other types of fuzzy decision-making problems. Several future research directions are put forward: (1) other decision-making methods in the context of PFHSs can be tested such as the LNMNAP method, and (2) new aggregation operators based on PFHSs is another direction.

Table 10 Dominance degree for \( Z_i \) and different \( \lambda \)

| State | \( \lambda \) | Alternative | \( \sqrt{\frac{\sum_{j=1}^{m} c_{ij}(d_{ij} - d_{ij})}{\sum_{j=1}^{m} c_{ij}}} \) | \( \frac{-1}{\theta} \sum_{j=1}^{m} c_{ij} \times (d_{ij} - d_{ij})/c_{ij} \) |
|-------|-------------|-------------|-----------------|-----------------|
| \( Z_1 \) | \( \lambda = 1 \) | \( A_1 \) | 0.105 0.069 0.032 0.000 0.000 | 0.000 0.000 0.000 0.000 |
| | | \( A_2 \) | 0.098 0.067 0.014 0.009 0.000 | 0.000 0.000 0.000 0.000 |
| | | \( A_3 \) | 0.093 0.025 0.015 0.000 0.000 | 0.000 0.000 0.000 0.000 |
| \( \lambda = 2 \) | \( A_1 \) | 0.208 0.130 0.062 0.000 0.000 | 0.000 0.000 0.000 0.000 |
| | | \( A_2 \) | 0.194 0.126 0.035 0.065 0.030 | 0.000 0.000 0.217 0.549 |
| | | \( A_3 \) | 0.088 0.052 0.102 0.000 0.000 | 0.000 0.000 0.000 0.573 |
| \( Z_2 \) | \( \lambda = 1 \) | \( A_1 \) | 0.074 0.078 0.037 0.007 0.000 | 0.000 0.000 0.000 0.000 |
| | | \( A_2 \) | 0.148 0.017 0.020 0.000 0.000 | 0.000 0.000 0.210 0.460 |
| | | \( A_3 \) | 0.084 0.094 0.060 0.000 0.000 | 0.000 0.233 0.090 0.185 |
| \( \lambda = 2 \) | \( A_1 \) | 0.166 0.149 0.083 0.024 0.000 | 0.000 0.000 0.353 0.656 |
| | | \( A_2 \) | 0.251 0.054 0.044 0.000 0.000 | 0.000 0.000 0.362 0.416 |
| | | \( A_3 \) | 0.189 0.173 0.122 0.000 0.000 | 0.000 0.362 0.416 0.336 |
| \( Z_3 \) | \( \lambda = 1 \) | \( A_1 \) | 0.011 0.000 0.000 0.000 0.000 | 0.000 0.000 0.000 0.000 |
| | | \( A_2 \) | 0.140 0.065 0.052 0.011 0.003 | 0.000 0.000 0.000 0.000 |
| | | \( A_3 \) | 0.110 0.094 0.065 0.012 0.000 | 0.000 0.000 0.000 0.000 |
| \( \lambda = 2 \) | \( A_1 \) | 0.031 0.000 0.000 0.000 0.000 | 0.000 0.000 0.000 0.000 |
| | | \( A_2 \) | 0.179 0.179 0.105 0.029 0.015 | 0.000 0.000 0.000 0.000 |
| | | \( A_3 \) | 0.216 0.156 0.142 0.039 0.000 | 0.000 0.000 0.000 0.000 |

Table 11 Comprehensive dominance degree in different \( Z_i \) and \( \lambda \)

| State | \( \lambda \) | \( \phi(A_1,A_i) \) | \( \phi(A_2,A_i) \) | \( \phi(A_3,A_i) \) | \( \phi(A_1,A_-) \) | \( \phi(A_2,A_-) \) | \( \phi(A_3,A_-) \) |
|-------|-------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| \( Z_1 \) | \( \lambda = 1 \) | -1.661 | -0.941 | -1.151 | 0.206 | 0.187 | 0.132 |
| | \( \lambda = 2 \) | -2.368 | -1.163 | -1.474 | 0.400 | 0.450 | 0.242 |
| \( Z_2 \) | \( \lambda = 1 \) | -1.695 | -1.227 | -1.002 | 0.196 | 0.185 | 0.238 |
| | \( \lambda = 2 \) | -2.086 | -1.778 | -1.437 | 0.422 | 0.349 | 0.484 |
| \( Z_3 \) | \( \lambda = 1 \) | -1.973 | -1.255 | -0.301 | 0.011 | 0.271 | 0.282 |
| | \( \lambda = 2 \) | -2.762 | -1.583 | -0.533 | 0.031 | 0.506 | 0.553 |

Table 12 Overall dominance value in different \( Z_i \) and \( \lambda \)

| State | \( \lambda \) | \( \Phi(A_1) \)(Rank) | \( \Phi(A_2) \)(Rank) | \( \Phi(A_3) \)(Rank) |
|-------|-------------|-----------------|-----------------|-----------------|
| \( Z_1 \) | \( \lambda = 1 \) | 0.000 (3) | 1.000 (1) | 0.622 (2) |
| | \( \lambda = 2 \) | 0.000 (3) | 1.000 (1) | 0.587 (2) |
| \( Z_2 \) | \( \lambda = 1 \) | 0.000 (3) | 0.622 (2) | 1.000 (1) |
| | \( \lambda = 2 \) | 0.000 (3) | 0.331 (2) | 1.000 (1) |
| \( Z_3 \) | \( \lambda = 1 \) | 0.000 (3) | 0.503 (2) | 1.000 (1) |
| | \( \lambda = 2 \) | 0.000 (3) | 0.601 (2) | 1.000 (1) |
The radar diagram showing the result of the different parameter $\lambda$ in status $Z_1$, $Z_2$, and $Z_3$.

**Fig. 4** Ranking outcomes of parameter $\lambda$ for state $Z_i$

### Table 13 The overall dominance value using another method [29]

| State | $\lambda$ | $\Phi(A_1)$ (Rank) | $\Phi(A_2)$ (Rank) | $\Phi(A_3)$ (Rank) |
|-------|------------|---------------------|---------------------|---------------------|
| $Z_1$ | $\lambda = 1$ | 0.862 (2) | 1.000 (1) | 0.000 (3) |
|       | $\lambda = 2$ | 0.754 (2) | 1.000 (1) | 0.000 (3) |
| $Z_2$ | $\lambda = 1$ | 0.166 (2) | 1.000 (1) | 0.000 (3) |
|       | $\lambda = 2$ | 1.000 (1) | 0.129 (2) | 0.000 (3) |
| $Z_3$ | $\lambda = 1$ | 0.000 (3) | 0.047 (2) | 1.000 (1) |
|       | $\lambda = 2$ | 0.003 (2) | 0.000 (3) | 1.000 (1) |

### Table 14 Comparison results between the method in [29] and the proposed method

| State | $\lambda$ | The method in [29] | The method proposed in this paper |
|-------|------------|---------------------|----------------------------------|
| $Z_1$ | $\lambda = 1$ | $A_2 > A_1 > A_3$ | $A_2 > A_3 > A_1$ |
|       | $\lambda = 2$ | $A_2 > A_1 > A_3$ | $A_2 > A_3 > A_1$ |
| $Z_2$ | $\lambda = 1$ | $A_2 > A_1 > A_3$ | $A_3 > A_2 > A_1$ |
|       | $\lambda = 2$ | $A_1 > A_2 > A_3$ | $A_3 > A_2 > A_1$ |
| $Z_3$ | $\lambda = 1$ | $A_3 > A_2 > A_1$ | $A_3 > A_2 > A_1$ |
|       | $\lambda = 2$ | $A_3 > A_2 > A_1$ | $A_3 > A_2 > A_1$ |

### Table 15 The overall dominance value using another method [31]

| State | $\lambda$ | $\Phi(A_1)$ (Rank) | $\Phi(A_2)$ (Rank) | $\Phi(A_3)$ (Rank) |
|-------|------------|---------------------|---------------------|---------------------|
| $Z_1$ | $\lambda = 1$ | 0.000 (3) | 0.470 (2) | 1.000 (1) |
|       | $\lambda = 2$ | 0.000 (3) | 1.000 (1) | 0.082 (2) |
| $Z_2$ | $\lambda = 1$ | 0.837 (2) | 0.000 (3) | 1.000 (1) |
|       | $\lambda = 2$ | 0.286 (2) | 0.000 (3) | 1.000 (1) |
| $Z_3$ | $\lambda = 1$ | 0.000 (3) | 1.000 (1) | 0.329 (2) |
|       | $\lambda = 2$ | 0.231 (2) | 1.000 (1) | 0.000 (3) |
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