CONDITIONS OF A SINGLE-MODE RIB CHANNEL WAVEGUIDE BASED ON DIELECTRIC TiO\textsubscript{2}/SiO\textsubscript{2}

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Abstract

In this paper, we propose conditions for the design of a single-mode rib channel waveguide based on dielectric materials such as titanium dioxide (TiO\textsubscript{2}) and silicon dioxide (SiO\textsubscript{2}) for the 0.633-\textmu m visible light. We also design Y-splitter structures, which show high-degree optical confinement and low bend losses at various radii of curvatures. Small radii of curvatures are extremely desirable in integrated photonics as they permit decreasing the dimensions but can also potentially reduce power consumption in the active devices.

Keywords: single mode, rib channel waveguide, titanium dioxide, silicon dioxide, beam propagation method.

Introduction

Optical communications through fiber have long been the technology of choice for high-speed long distance data links [1]. Progressively, as the capacity requirements have increased, the optical links have developed into shorter distance applications, such as fiber-to-the-home, local area network, and even into fiber optic interconnects between boards and cabinets. In the long run, optics would be used to interconnect the integrated circuits on a board or even to be used in intra-chip interconnects. That is, electrical interconnects, which have dominated since the infancy of electronics, are likely to be substituted with optical interconnects in some cases [2]. Integrated optics devices are based on the processing of light confinement in optical structures called optical waveguides. It allows the confinement of light by total internal reflection, which takes place when the high index medium is surrounded by the low index medium [3–8]. The most significant passive elements in the integrated optics are the slab waveguides in the side region. Therefore, a criterion should be worked out for the proportional sizes of transversal dimensions in order to ensure the single mode propagation [13]. In this paper, conditions for single mode rib channel waveguide based on titanium dioxide and silicon dioxide are proposed; afterwards, the Y-splitter structure is also designed which shows the high degree of confinement and low bend losses at low radii of curvature.

These kind waveguides consist of three layers of dielectric materials. Layer 1 has a thickness of \( H \) with a refractive index of \( n_1 \). The layer is then etched while covering the rib section of the waveguide with the help of a metal mask; this gives rise to a slab of height \( h \). Layer 1 has a refractive index of \( n_1 \). Layer 2 and layer 3 have a semi-finite thickness and index of \( n_2 \) and \( n_3 \), respectively. We shall assume that \( n_1 > n_2 \) and \( n_1 > n_3 \). So that total internal reflection can occur at each interface. Layer 1 is referred to as the guiding layer, while layer 2 and 3 are a substrate and the cladding layer, respectively.

A guiding of this type can be formed simply by depositing a high index guiding layer onto a polished substrate. In our case, the cladding layer is air. Because of this geometry, it is normally described as an asymmetric rib waveguide and take \( n_1 > n_2 > n_3 \). For the modeling of such waveguides, we proposed TiO\textsubscript{2} (2.5836 at 0.633 \textmu m) and SiO\textsubscript{2} (1.4570 at 0.633 \textmu m) as high and low refractive index materials, respectively. The refractive index difference between two material is quite high \( \Delta n = 1.1266 \) which can be helpful in confining the light at the higher degrees of bends. The materials in which the guided light propagates must elude scattering and absorption losses in the wavelength range of interest [14].

Fig. 1 shows the cross-sectional view of the rib waveguide, where \( h \) is the height of the slab, \( H \) is the slab height plus rib height and \( W \) is the width of the rib. The structuration of the layer can be done with different techniques [15].
Conditions for single mode straight channel rib waveguide

Nowadays, an increasing number of optical modulators, filters and other functions relevant to telecommunication networks have been proposed as integrated or embedded in dielectric rib/ridge waveguides [16, 17]. Many of them share the widespread feature of being based on the propagation of the light beam inside a waveguide which has been designed to sustain only its fundamental mode of propagation to allow lower insertion losses when coupled to optical fibres. For the modeling of a single mode straight channel rib waveguide, the parameters such as \( h \) (height of slab), \( H \) (height of rib) and \( W \) (width of the rib) are considered. All the bounded modes are determined at \( 0.633 \mu m \) by using beam propagation method (BPM). The thickness of \( H \) is kept in the range of 100–1000 nm limited to the deposition techniques. Table 1, shows the parameters of waveguide used in the simulations and the type of waveguide obtained by it.

The ratios between \( (h, H) \) and \( (W, H) \) are plotted in Fig. 2 which represents the dimensions that can be used to design single and multi-mode rib channel waveguides. It can be seen that the region defined by the grey squares are the dimensions of waveguides that can only support a fundamental single mode and the region which is covered by black dots is useful to design multi-mode waveguides. Therefore, this graph can offer an approximation for indicating the dimensions of single mode waveguide based on these materials.

| No. of Simul. | \( h \) (nm) | \( H \) (nm) | \( W \) (nm) | \( h/H \) | \( W/H \) | Waveguide type |
|---------------|-------------|-------------|-------------|----------|----------|----------------|
| 1             | 100         | 1000        | 5000        | 0.1      | 5        | Single         |
| 2             | 100         | 500         | 2250        | 0.2      | 4.5      | Multi          |
| 3             | 100         | 300         | 1300        | 0.3      | 4        | Single         |
| 4             | 100         | 250         | 875         | 0.4      | 3.5      | Single         |
| 5             | 100         | 200         | 600         | 0.5      | 3        | Single         |
| 6             | 100         | 170         | 400         | 0.6      | 2.5      | Single         |
| 7             | 100         | 140         | 280         | 0.7      | 2        | Single         |
| 8             | 100         | 125         | 180         | 0.8      | 1.5      | Single         |
| 9             | 100         | 110         | 110         | 0.9      | 1        | Single         |
| 10            | 100         | 100         | 50          | 1        | 0.5      | Single         |
| 11            | 100         | 500         | 1000        | 0.2      | 2        | Single         |
| 12            | 100         | 200         | 400         | 0.5      | 2        | Single         |
| 13            | 100         | 140         | 140         | 0.7      | 1        | Single         |
| 14            | 100         | 125         | 375         | 0.8      | 3        | Single         |
| 15            | 100         | 170         | 670         | 0.6      | 4        | Single         |
| 16            | 100         | 1000        | 3000        | 0.1      | 3        | Multi          |
| 17            | 100         | 1000        | 4000        | 0.1      | 4        | Multi          |
| 18            | 100         | 150         | 625         | 0.4      | 2.5      | Single         |
| 19            | 100         | 250         | 1375        | 0.4      | 5.5      | Single         |
| 20            | 100         | 200         | 1100        | 0.5      | 5.5      | Single         |
| 21            | 100         | 1000        | 1000        | 0.1      | 1        | Single         |
| 22            | 100         | 300         | 300         | 0.3      | 1        | Single         |
| 23            | 100         | 250         | 250         | 0.4      | 1        | Single         |
| 24            | 100         | 200         | 900         | 0.5      | 4.5      | Single         |
| 25            | 100         | 500         | 1500        | 0.2      | 3        | Multi          |
| 26            | 100         | 300         | 1600        | 0.3      | 5        | Single         |
| 27            | 100         | 125         | 560         | 0.8      | 4.5      | Single         |
| 28            | 100         | 1000        | 2000        | 0.1      | 2        | Multi          |
| 29            | 100         | 500         | 2750        | 0.2      | 5.5      | Multi          |
| 30            | 100         | 300         | 100         | 0.3      | 3        | Single         |
| 31            | 100         | 500         | 500         | 0.2      | 1        | Single         |
| 32            | 100         | 300         | 670         | 0.3      | 2        | Single         |
| 33            | 100         | 200         | 1000        | 0.45     | 4.5      | Single         |
Single mode Y-splitter structure

After proposing the conditions of straight rib channel waveguide, the design for the balanced Y-splitter structure is proposed. Several Y-splitter structures with varying radii of curvatures are simulated. The waveguide dimensions (Simulations: 1–6) are kept constant. The size of Y-splitter is fixed to 8 mm but with increasing radii of curvature in each simulation. The schematic of the Y-splitter design based on TiO2/SiO2 is shown in Fig. 4. The length of the input straight channel waveguide is kept as long as possible depending on the design. This helps in removing the fluctuations and clean the propagating mode. The detail about the parameters is shown in Table 2.

![Fig. 4. Schematic of 8 mm long Y-splitter structure with varying distance between two arms ranges from 2–12 µm](image)

The propagation of light intensity in one arm of 6 different Y-splitters with a varying radius of curvature, R is plotted in Fig. 5(a). Since the Y-splitter structure is symmetric, therefore the power in each arm is equal. By keeping the optimum separations, coupling effect between two arms can be avoided. An optimum value of the radius of curvature should be selected in order to provide a smooth bending to the propagation light. S-bend waveguides with fixed radius of curvature R range between 93–560 mm are used to design the Y-splitters. S-bend waveguides are important as input/output waveguides for directional couplers and as waveguide path transformers in various circuits.

The fundamental mode of a straight channel rib waveguide was calculated and used as a launch field for Y-splitter. Let’s consider, the launch field has an intensity of 1 a.u. The Y-splitter with a separation of 10 µm between its arms contains the maximum energy of 0.491 a.u/arm. The lowest energy of 0.465 a.u/arm was obtained in the case of Y-splitter with 4 µm of separation between its arms. This shows an energy difference of nearly 3% if Y-splitters are designed with R between 93–560 mm as shown in Fig. 5(b).

### Table 2. Y-splitter structure of 8000 µm long with various radius of curvature

| No. of simul. | h (µm) | H (µm) | W (µm) | Length of input straight waveguide, \(L_{\text{in}}\) (µm) | Length of bend waveguide, \(L_{\text{bend}}\) (µm) | Length of output straight waveguide, \(L_{\text{out}}\) (µm) | Separation between two arms, \(L_{\text{s}}\) (µm) | Radii of curvature, \(R\) (mm) |
|---------------|--------|--------|--------|-----------------------------------------------|---------------------------------------------|-----------------------------------------------|---------------------------------------------|-------------------|
| 1             | 0.05   | 0.25   | 0.5    | 2000                                         | 1500                                        | 4500                                          | 2                                           | 560               |
| 2             | 0.05   | 0.25   | 0.5    | 2000                                         | 1500                                        | 4500                                          | 4                                           | 280               |
| 3             | 0.05   | 0.25   | 0.5    | 2000                                         | 1500                                        | 4500                                          | 6                                           | 188               |
| 4             | 0.05   | 0.25   | 0.5    | 2000                                         | 1500                                        | 4500                                          | 8                                           | 140               |
| 5             | 0.05   | 0.25   | 0.5    | 2000                                         | 1500                                        | 4500                                          | 10                                          | 110               |
| 6             | 0.05   | 0.25   | 0.5    | 2000                                         | 1500                                        | 4500                                          | 12                                          | 93                |

Out of six simulations shown in Fig. 5, we choose the best design of the Y-splitter and plotted its mode profile at the output as shown in Fig. 6(a). The separation between the two arms was at 20 µm to avoid any possible evanescent field coupling between two arms. The optical field at the output of the matched S-bends and in the subsequent straight waveguide section is undistorted. As a consequence, the fields at the Y-branch output are balanced as demonstrated by the horizontal cross-section of the mode as shown in Fig. 6(b). Moreover, there is no leakage of the mode in the substrate as can be seen in Fig. 6(c), where mode has an FWHM of 0.1692 µm which is nearly equal to the height of the rib.

Fig. 5. Variation of launch power a) 8 mm long Y-splitter structure with varying distance between two arms ranges from 2–12 µm b) Magnified image of the power in the propagation length from 4–5 mm

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We proposed the conditions of a single mode rib channel waveguide based on TiO$_2$ and SiO$_2$ dielectric materials at 0.633 µm visible light by optimizing different parameters of the waveguide with the help of Beam Prop software. These dielectric materials have high refractive index contrast which makes them an outstanding platform for the realization of S-bend and Y-splitters with the small radii of curvature. Based on these results, many optical elements such as S-bend, Y-splitter can be realized which can be used for different optical applications. Moreover, the Y-splitter structures are designed which shows the high degree of optical confinement and low bend losses at various radii of curvatures. Small radii of curvatures are extremely desirable in integrated photonics as they permit decreasing the dimensions but can also potentially reduce the power consumption in the active devices.

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