Deep generative-contrastive networks for facial expression recognition

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Abstract

As the expressive depth of an emotional face differs with individuals, expressions, or situations, recognizing an expression using a single facial image at a moment is difficult. One of the approaches to alleviate this difficulty is using a video-based method that utilizes multiple frames to extract temporal information between facial expression images. In this paper, we attempt to utilize a generative image that is estimated based on a given single image. Then, we propose to utilize a contrastive representation that explains an expression difference for discriminative purposes. The contrastive representation is calculated at the embedding layer of a deep network by comparing a single given image with a reference sample generated by a deep encoder-decoder network. Consequently, we deploy deep neural networks that embed a combination of a generative model, a contrastive model, and a discriminative model. In our proposed networks, we attempt to disentangle a facial expressive factor in two steps including learning of a reference generator network and learning of a contrastive encoder network. We conducted extensive experiments on three publicly available face expression databases (CK+, MMI, and Oulu-CASIA) that have been widely adopted in the recent literatures. The proposed method outperforms the known state-of-the-art methods in terms of the recognition accuracy.

1. Introduction

Facial expressions are a primary modality to understand the emotional status of an individual. The expression provides a useful contextual clue for social communication [11]. However, individuals do not always clearly reveal their facial expressions. When an individual reveals an ambiguous facial expression, a human may have an experience to compare his/her expression with other expressions observed in past in order to extract their facial expression differences. The related evidence is found in the literature of brain sciences. According to [4, 5, 11], an individual can discern various facial expressions by recalling the memorized face shapes of a shown person. The neural pathways for detecting changeable aspects of faces (e.g., eye movements and emotional expressions) and for memorizing the unique face shape are separately distributed [4, 11]. These two processes are interacted in the core system of the brain [5, 11].

We attempt to utilize a reference face image that indicates the memorized unique face in the brain to discriminate a facial expression input in a deep neural network framework (see Figure 1). We assume that an expression factor can be extracted from the contrastive characteristics between the given image and the reference image. The reference image for an individual identity, however, is not always available in the wild. We start from the assumption that there is a generative artificial neural network that can be used to infer a reference image from the given facial ex-
3. Contrastive facial representation learning

Consider an input image matrix $X$ and a reference image matrix $X_r$ that are elements of a given set of image matrices $\mathcal{I} = \{X_i \in \mathbb{R}^{h \times w} \forall i\}$. The corresponding expression label is denoted by $y \in \mathbb{R}$ and $y_r \in \mathbb{R}$ respectively. In a real
world, an expressive face might be changed from a reference ground face (due to emotional changes that incur facial muscle movements \[25\]). We define a relationship between two images with a hidden factor denoted by \( \epsilon \in \mathbb{R}^{h \times w} \) formally as follows:

\[
X := X_r + \epsilon \quad (1)
\]

where the addition indicates operations for facial expression change\(^1\).

As a facial expression is not always apparently represented as an absolute value, a quantity of expression change obtained by comparing with a reference image might be useful. An expression image with a very small change could be recognized via difference maps (e.g., a pixel-wise distance and optical flows). As a human keeps a neutral-like or less-expressive face most of the time, that face image could be considered as the reference image.

A representation of a difference between expression images can appear in various ways. A simple approach is to compare image pixels of the faces. However, owing to distortions between the images (e.g., distortions by an affine transform), comparing the images at the pixel level is not effective. For example, a small translation in the image level might return large pixel-wise errors even though a human face shows no expression changes.

\(^1\)Since the change of expression should be measured in the same subject, we assumed that a hidden expression factor is represented within the same subject, i.e., if a subject term \( s \) is added at the Equation (1):

\[X_s := X_{sr} + \epsilon.\]

In this paper, we omit the term \( s \) for a simplicity in the notation.

3.1. Representation of a difference between facial expressions via networks

The representation of the difference (“contrastive representation”) can be better extracted at the feature level, but not at the pixel level. The feature-wise representation can offer an invariance towards distortions (e.g., translation, scale, or rotation).

We employ a contrastive representation in the networks to extract a latent difference factor between expressions. Consider a pair of images \( \{X, X_r\} \in \mathcal{I} \), where \( X \) is an input sample and \( X_r \) is a reference sample. Let \( \text{En} \) (abbreviation of an encoder) be a transform function used to map an input matrix to the embedding space \( \bullet \rightarrow \text{En}(\bullet) : \mathcal{I} \rightarrow \mathbb{R}^p \). In the transformed space, a latent factor in the feature level (\( \delta \)) can be represented as follows:

\[
\delta := d(\text{En}(X), \text{En}(X_r)), \quad (2)
\]

where \( d(\bullet, \bullet) \) is an element-wise distance formulation and \( \delta \in \mathbb{R}^p \). In this paper, we adopt a distance \( \|\text{En}(X)_j - \text{En}(X_r)_j\| \in \mathbb{R} \) of the \( j \)-th element of the feature vector, \( \forall j = 1, \ldots, p \) for \( d(\bullet, \bullet) \).

In the contrastive representation of “expressiveness,” we expect that other factors (e.g., individual’s identity, pose, and etc.) than the expression will be eliminated. The contrastive representation \( \delta \) is used for a discriminative task.

3.2. Generating reference image

The reference face image, such as less-expressive face image of an individual, may not be available in the test
phase. In this paper, therefore, we propose to generate the reference face using convolutional encoder-decoder networks. To estimate a reference face transformed from an expression face, we apply the concept of the denoising autoencoder (DAE). In the DAE, a term corresponding to corruption, i.e., a Gaussian distribution, added to the original input is eliminated via learning\(^2\) [3]. In this section, we assume that the term corresponding to corruption should not be limited to a specific probability distribution. There might be a latent model (or unknown transform) that makes a face with a certain expression appear to be a reference face. Without a definition of the latent distribution, in this paper, the model is represented using encoder-decoder networks. By disentangling facial expressive factors in feature learning, hence, information that is irrelevant or of negligible use for the discriminative purposes could be discarded [2].

### 3.3. Generative and contrastive networks

In this section, we show how the generated reference image can be used in deep networks. Multiple objectives are adopted to optimize parameters of the networks to generate a good contrastive representation.

As shown in Figure 2 (f) and 3, a loss function (\(\mathcal{L}\)) of the proposed networks consists of three kinds of objectives. Formally, the loss function is written as follows:

\[
\mathcal{L} = \mathcal{L}_{Cl} + \lambda_S \mathcal{L}_{Con} + \lambda_R \mathcal{L}_{Rec} \tag{3}
\]

where \(\mathcal{L}_{Cl}\) denotes a discriminative loss function, \(\mathcal{L}_{Con}\) denotes a contrastive loss function, and \(\mathcal{L}_{Rec}\) denotes a reconstruction loss function. \(\lambda_S, \lambda_R \in \mathbb{R}\) indicates a weight.

The main purpose of the proposed networks is to classify a facial expression in the given input. For the discriminative objective \(\mathcal{L}_{Cl}\), we adopt the cross entropy loss function which is widely used for the classification task. Consider a pair of features \(\{\text{En}_2(X), \text{En}_2(\hat{X}_r)\}\) extracted from encoder layers \(\text{En}_2\), where a subscript 2 at \(\text{En}_2\) indicates the second encoder layers (representation layers shown in Figure 3). A contrastive representation feature \(d(\text{En}_2(X), \text{En}_2(\hat{X}_r)) \in \mathbb{R}^p\) where \(d(\bullet, \bullet)\) is the element-wise distance and \(p > 0\) is used for the classification task.

For learning a contrastive representation, two learning objectives are deployed in the proposed networks: the first objective is contrastive metric learning (\(\mathcal{L}_{Con}\)) to enlarge or to diminish the distance between the two feature vectors, and the second is reconstruction learning (\(\mathcal{L}_{Rec}\)) for a better representation. Hence, the two objective functions are designed to jointly assist the classification task for realizing a good generalization performance.
Loss for contrastive metric learning in feature space.
The objective of the loss $L_{\text{Contr}}$ is to optimize a similarity between two features $\{\text{En}_2(X), \text{En}_2(X')\}$ according to an expression label. If the expression labels of $X$ and $X'$ are not identical, the function optimizes to obtain dissimilar features within a predefined margin; if the expressions are identical, it optimizes to similar features. Hence, the contrastive loss [10] is adopted for $L_{\text{Contr}}$ in a feature space as follows:

$$L_{\text{Contr}} = \frac{1}{2} \left( \max(0, m - S(\text{En}_2(X), \text{En}_2(\hat{X}))) \right)^2 \tag{4}$$

$$+ (1 - \alpha) \frac{1}{2} \left( S(\text{En}_2(X), \text{En}_2(X')) \right)^2 \tag{5}$$

where $\alpha = 1$ if the labels of a pair $\{X, \hat{X}\}$ are not the same, $\alpha = 0$ otherwise, $S(\text{En}_2(X), \text{En}_2(X')) = \|\text{En}_2(X) - \text{En}_2(X')\|_2 \in \mathbb{R}$ is a similarity measure, and $m > 0$ is a margin. A feature space is defined as $(\bullet \rightarrow \text{En}_2(\bullet) : \mathcal{X} \rightarrow \mathbb{R}^P)$ at the encoder layers.

Loss for generation and representation. The main objectives of the loss $L_{\text{Recon}}$ are two-fold: one is to generate a reference image, and the other is to supplement to represent a good contrastive feature in the embedding layer ($\text{En}_2(\bullet)$). Hence, a reconstruction loss ($L_{\text{Recon}}$) can be represented as a weighted summation of three terms as follows:

$$L_{\text{Recon}} = \lambda_{G,r}L_{\text{Gen},r} + \lambda_{R,r}L_{\text{Recon},r} + \lambda_{R,i}L_{\text{Recon},i} \tag{6}$$

where of the subscripts of $L_{*,*}$, the first one $*_r \in \{\text{Gen}, \text{Recon}\}$ indicates the stage for a generation ($\text{Gen}$) or a reconstruction ($\text{Recon}$) (shown in Figure 3). The second subscript $*_r \in \{r, i\}$, indicates a target: $r$ for a reference image, and $i$ for an input image.

$$L_{\text{Gen},r} = \frac{1}{2} \|X_r - \text{De}_1,r(\text{En}_1(X))\|^2_2 \tag{7}$$

$$L_{\text{Recon},r} = \frac{1}{2} \|X_r - \text{De}_2,r(\text{En}_2(\text{Generator}(X)))\|^2_2 \tag{8}$$

$$L_{\text{Recon},i} = \frac{1}{2} \|X - \text{De}_2,i(\text{En}_2(X))\|^2_2 \tag{9}$$

where $\text{Generator}(X) = \text{De}_1,r(\text{En}_1(X))$ is learned to estimate $X_r$.

4. Experiments

In this section, we describe the experiments conducted to compare the proposed method with the state-of-the-arts on three publicly available face expression databases (CK+, MMI, and Oulu-CASIA) that are widely adopted in the literatures [9, 12, 13, 14, 15, 16, 17, 18, 19, 23, 25, 26, 27, 29].

4.1. Networks model and settings

All models used in different databases share exactly the same architecture (shown in Figure 3), including encoder-decoder networks depicted in Table 1. All parameter settings are shared through the databases with the same value. The encoder-decoder networks in Table 1 are pre-trained with the reconstruction task using the CASIA-WebFace database [6], and three convolutional layers in the encoder are adopted at Encoder$_1$ ($\text{En}_1$) of the proposed generative-contrastive networks (GCNet) shown in the Figure 3. The baseline CNN consisting of three convolutional layers and two inner-product (FC) layers are pre-trained with the identification task using the same database, and convolutional layers are adopted at Encoder$_2$ ($\text{En}_2$). During the training of the proposed networks, the learning rate at layers of the decoder networks is set to 10 during fine-tuning. The number of outputs at the first fully-connected layer (inner-product) is empirically determined by $(0.5 \times \text{Wsize})^2 * nlayers/(2^{n\text{layers}})$ where we set Wsize = 64, nlayers = 3. This is intended that a dimensionality of the vector decreases smoothly as the number of (conv./pool) layers increases. $\frac{1}{\text{Wsize}}$ is related to a pooling size ($\frac{1}{2}$) at each layer. The dropout is applied before this fully-connected layer with a ratio of 0.5. After the FC-layer, a softmax layer is connected with the number of outputs corresponding to the number of classes. We arbitrarily set $\lambda_S = 1, \lambda_{G,r} = 1, \lambda_{R,r} = 0.25, \lambda_{R,i} = 0.25$ for each loss function. The maximum iteration is set to $3 \times 10^5$.

Our models are trained with ‘Nesterov’ optimization using an ‘inverse’ learning policy, a base learning rate of 0.001, a momentum of 0.9, a gamma term of 0.75, a weight decay of 0.0001, and a mini-batch size of 64. The proposed network model is implemented on Python and the deep learning framework Caffe and run using the NVIDIA Tesla K80 GPU.

To avoid over-fitting, we applied data augmentation during the training phase. We used input images on a gray level (1 channel) where a facial region is cropped, normalized based on 5 points (eyes, the end of a nose, and two ends of lips) and resized into $66 \times 66$. The resized image is cropped again with the size of $64 \times 64$ at a random location. Each cropped image is manipulated using 2D affine transform such as scaling, rotation, and intensity multiplication, in addition to random flipping.

4.2. Databases and protocols

CK+ Database [20] This database is widely adopted in the benchmark for facial expression recognition tasks. This database consists of 593 sequences with 123 individuals. The images are captured expression transitions from a neutral face to peak facial expression acted by an individual. The 327 valid sequences with 118 individuals that maintain discrete emotion labels such as ‘Anger, Contempt, Dis-
gust, Fear, Happy, Sad, and Surprise” are adopted for an experiment. We divide the valid sequences into ten different subsets with individual-independent way. According to individual ID in the database, individuals are grouped by sampling in ID ascending order with ten even intervals first. One subset out of ten subsets is used for validation (test), the remains are used for training. This procedure is repeated ten times. This 10-fold cross-validation follows the previous works [13, 19].

**MMI Database** [24] This database consists of 312 sequences from 30 individuals with six basic expressions (Contempt included in the CK+ database is excluded). We selected 205 sequences captured in a front view. Each sequence starts from a neutral face, and shows a peak expression within a single expression type in the middle of the sequence. At the end, it returns to a neutral face again. As a peak expression frame number is not given, we selected it manually. Similar to the CK+ database settings, we divided the MMI database into ten different individual independent subsets. Consequently, 10-fold cross validation was conducted. This database includes individuals who pose expressions non-uniformly, wear glasses/caps, and have mustaches/ head movements. Therefore, the facial expression recognition task is relatively challenging. Moreover, the small number of sequences and individuals makes it difficult to achieve a good generalization performance. This database could be suitable to measure the recognition performance in realistic situations when compared to other databases.

**Oulu-CASIA VIS Database** [26] This database consists of 480 image sequences with 80 individuals. This database is captured under the visible (VIS) normal illumination conditions and is a subset of Oulu-CASIA NIR-VIS database. Each individual poses six basic expressions similar to MMI database. Similar to the CK+ database, the sequence starts from a neutral face and ends with peak facial expression within the same emotion category. As done with the two databases above, individual-independent 10-fold cross-validation is conducted.

### 4.3. Quantitative results

Among all the compared databases, the proposed methods outperform the state-of-the-art methods including handcraft based methods (LBP-TOP [27] and HOG 3D [15]), video-based methods (MSR [23], TMS [12], STM-ExpLet [19], and DTAGN-Joint [13]) that utilize temporal information, FAU inspired methods (AURF [16], AUDB [17]), and CNN-based methods (3D-CNN [19], 3D-CNN-DAP [19], zero-bias CNN+AD [14], and DTAGN-Joint [13]).

In the CK+ database, seven expressions and a neutral image are included. We conducted experiments for seven expressions as well as eight expressions (seven expressions and a neutral face). For the seven expressions cases shown in Table 2, the proposed methods (GCNet_{S1R0}, GCNet_{S1R1}, GCNet_{S0R1}, and GCNet_{S0R1}) show a better recognition performance than that of all compared state-of-the-arts including hand-craft feature based methods (LBP-TOP [27] and HOG 3D [15]), CNN-based methods (3D-CNN [19], 3D-CNN-DAP [19], and DTAGN-Joint [13]), and video-based methods (MSR [23], TMS [12], STM-ExpLet [19], and DTAGN-Joint [13]). For cases of the eight expressions shown in Table 3, the proposed methods (GCNet_{S0R0}, GCNet_{S1R0}, GCNet_{S0R1}, and GCNet_{S1R1}) show a better recognition performance than the compared deep learning-based methods including FAU aware methods (AURF [16], AUDB [17]) and a CNN-based method (Zero-bias CNN+AD [14]). When a loss function of contrastive metric learning is eliminated (GCNet_{S0R0} and GCNet_{S0R1}), we observed that the performance is degraded than that with a contrastive loss (GCNet_{S1R0} and GCNet_{S1R1}) on the CK+ database.

In the MMI database, similar to the case of the CK+ database, the proposed methods show a higher accuracy value than that of the state-of-the-arts including CNN-based methods (3D-CNN-DAP [19] and DTAGN-Joint [13]) and video-based methods (STM-ExpLet [19] and DTAGN-Joint [13]) as shown in Table 4. The methods (STM-ExpLet [19] and DTAGN-Joint [13]) that acquire temporal information from multiple images show relatively higher accuracy performance than other methods. Even though the proposed methods show a better recognition performance than these compared methods, the recognition accuracy of the proposed methods on the MMI database is relatively less compared to that on other databases (CK+ and Oulu-CASIA VIS).

| Encoder (3 convolutional layers) |      |      |      |      |      |      |
|---------------------------------|------|------|------|------|------|------|
| (5 × 5, 32) Conv. BNorm ReLU, (5 × 5) MaxPool |      |      |      |      |      |      |
| (3 × 3, 64) Conv. BNorm ReLU, (3 × 3) MaxPool |      |      |      |      |      |      |
| (3 × 3, 96) Conv. BNorm ReLU, (3 × 3) MaxPool |      |      |      |      |      |      |

| Decoder (3 de-convolutional layers) |      |      |      |      |
|-------------------------------------|------|------|------|
| (3 × 3) MaxUnPool, (3 × 3, 32) DeConv. BNorm ReLU |      |
| (3 × 3) MaxUnPool, (3 × 3, 64) DeConv. BNorm ReLU |      |
| (5 × 5) MaxUnPool, (5 × 5, 1) DeConv. BNorm ReLU |      |

Table 1: Details of the convolutional encoder-decoder layers [22] embedded in the proposed networks. An encoder part consists of three convolutional layers (Conv.) which is followed by Batch Normalization (BNorm), ReLU, and Max Pooling layers. Correspondingly, a decoder part consists of three de-convolutional (transposed convolutional) layers. In a Conv and DeConv. layers, (5 × 5, 32) indicates that there is 32 sets of 5 × 5 filters. In MaxPool and MaxUnPool layers, (5 × 5) indicates a pooling window size.
Table 2: Averaged recognition accuracy (%) on the CK+ database, 7 expressions.

| Method                  | Accuracy (%) |
|-------------------------|--------------|
| LBP-TOP [27]            | 88.99        |
| HOG 3D [15]             | 91.44        |
| MSR [23]                | 91.4         |
| TMS (4-fold) [12]       | 91.89        |
| STM-ExpLet [19]         | 94.19        |
| DTAGN-Joint [13]        | 97.25        |
| 3D-CNN [18]             | 85.9         |
| 3D-CNN-DAP [18]         | 92.4         |
| CNN (baseline)          | 96.94        |
| Ours (GCNetS0R0)        | 97.08        |
| Ours (GCNetS1R0)        | 97.83        |
| Ours (GCNetS0R1)        | 97.53        |
| Ours (GCNetS1R1)        | 97.93        |

Table 3: Averaged recognition accuracy (%) on the CK+ database, 8 expressions.

| Method                  | Accuracy (%) |
|-------------------------|--------------|
| AURF [16]               | 92.22        |
| AUDB [17]               | 93.70        |
| Zero-bias CNN+AD [14]   | 96.4         |
| CNN (baseline)          | 95.47        |
| Ours (GCNetS0R0)        | 95.74        |
| Ours (GCNetS1R0)        | 96.75        |
| Ours (GCNetS0R1)        | 96.50        |
| Ours (GCNetS1R1)        | 97.28        |

Table 4: Averaged recognition accuracy (%) on the MMI database, 6 expressions.

| Method                  | Accuracy (%) |
|-------------------------|--------------|
| LBP-TOP [27]            | 59.51        |
| HOG 3D [15]             | 60.89        |
| ITBN [25]               | 73.53        |
| CSPL [29]               | 75.12        |
| STM-ExpLet [19]         | 70.24        |
| DTAGN-Joint [13]        | 53.2         |
| 3D-CNN [18]             | 63.4         |
| 3D-CNN-DAP [18]         | 77.68        |
| CNN (baseline)          | 76.20        |
| Ours (GCNetS0R0)        | 78.86        |
| Ours (GCNetS1R0)        | 77.00        |
| Ours (GCNetS0R1)        | 81.53        |

Table 5: Averaged recognition accuracy (%) on the Oulu-CASIA VIS database, 6 expressions.

| Method                  | Accuracy (%) |
|-------------------------|--------------|
| LBP-TOP [27]            | 68.13        |
| HOG 3D [15]             | 70.63        |
| AdaLB [26]              | 73.54        |
| Atlases [9]             | 75.52        |
| STM-ExpLet [19]         | 74.59        |
| DTAGN-Joint [13]        | 81.46        |
| CNN (baseline)          | 83.96        |
| Ours (GCNetS0R0)        | 84.65        |
| Ours (GCNetS1R0)        | 86.39        |
| Ours (GCNetS0R1)        | 85.83        |
| Ours (GCNetS1R1)        | 86.11        |

4.4. Qualitative analysis

Small expression images In Figure 4, several examples of recognition errors on the small expression images are shown. Our proposed method shows approximately twice less recognition errors than baseline CNN method. However, both the baseline CNN and the proposed method still have a limitation to recognize the small (or ambiguous) expressions.

Visualization in the feature space To observe a discriminative distribution of the extracted features, we visualized the feature vectors from the first layer of the fully-connected layers of the proposed networks of the baseline CNN and our proposed networks. We visualize the 384 dimensional feature vectors using t-SNE [21]. The feature points of original images are scattered within a narrow region. The point distribution of the baseline CNN forms partially overlapped
Figure 5: Visualization of the extracted features using t-SNE: (a) a pixel value of the input images, (b) a feature vector of CNN (baseline), and (c) a feature vector of the proposed method (GCNet$^{S1,R1}$).

Patterns of the learned filters We observe the characteristics of the filters learned in the proposed networks. As shown in Figure 6, the encode filters learned by contrastive metric learning, (b), has more Gabor like edge and blob detection filters than (a). The decoder filters for the expression reconstruction, (e), show a simpler patterns than that for the reference image generator, (c), and the reconstruction decoder of a neutral image, (d), as shown in Figure 6.

Visualization of the response maps We observe the response maps resulted from generation and reconstruction layers of the proposed networks to understand what the networks have been conducted in the test phase. In Figure 7, a generated reference image, a reconstructed neutral image, and a reconstructed image of a given expression are shown. The generated reference image is affected by reconstruction and contrastive metric learning.

5. Conclusions

In this paper, we proposed facial expression recognition method based on contrastive representation learning. The contrastive representation is calculated in the embedding layer of deep networks by comparing a single given image with a reference image. The reference image is generated by deep generative (encoder-decoder) networks. This approach is useful especially if an expressive depth of an emotional face is varied among individuals, expressions, or situations. In our proposed networks, we attempted to disentangle a facial expressive factor directly. Disentangling of expression is conducted in two steps: 1) learning of a reference face by a generator network and 2) learning of a contrastive representation with a combination of contrastive and reconstruction objectives. Extensive experiments were conducted on three face expression databases that are publicly available and widely adopted in the literature. The proposed method outperforms the known state-of-the arts, including both single image and multiple-image based meth-
ods. This study could be extended to effectively detect and recognize small changes of facial expressions from sequential images.

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