FAR-INFRARED PROPERTIES OF SPITZER-SELECTED LUMINOUS STARBURSTS

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ABSTRACT

We present SHARC-2 350 μm data on 20 luminous z ~ 2 starbursts with S_{1.2mm} > 2 mJy from the Spitzer-selected samples of Lonsdale et al. and Fiolet et al. All the sources were detected, with S_{350μm} > 25 mJy for 18 of them. With the data, we determine precise dust temperatures and luminosities for these galaxies using both single-temperature fits and models with power-law mass–temperature distributions. We derive appropriate formulae to use when optical depths are non-negligible. Our models provide an excellent fit to the 6 μm–2 mm measurements of local starbursts. We find characteristic single-component temperatures T_I ≃ 35.5 ± 2.2 K and integrated infrared (IR) luminosities around 10^{12.9} ± 0.1 L_⊙ for the SWIRE-selected sources. Molecular gas masses are estimated at ≃4 × 10^{10} M_⊙ assuming κ_{350μm} = 0.15 m^2 kg^{-1} and a submillimeter-selected galaxy (SMG)-like gas-to-dust mass ratio. The best-fit models imply >2 kpc emission scales. We also note a tight correlation between rest-frame 1.4 GHz radio and IR luminosities confirming star formation as the predominant power source. The far-IR properties of our sample are indistinguishable from the purely submillimeter-selected populations from current surveys. We therefore conclude that our original selection criteria, based on mid-IR colors and 24 μm flux densities, provides an effective means for the study of SMGs at z ~ 1.5–2.5.

Key words: galaxies: high-redshift – galaxies: ISM – galaxies: photometry – galaxies: starburst – infrared: galaxies – submillimeter: galaxies

Online-only material: color figures, extended figure

1. INTRODUCTION

Star-forming galaxies release a significant fraction of their energy output at infrared (IR) and submillimeter wavelengths (λ ~ 5–1000 μm in the rest frame). The luminosities of starbursts, with star formation rates over 100 M_⊙ yr^{-1}, are almost exclusively carried at IR wavelengths. Whereas luminous and ultra-luminous infrared galaxies (LIRGs and ULIRGs) are extremely rare in the local universe, they are prevalent at higher redshifts (e.g., Le Floc’h et al. 2005; Caputi et al. 2007). By studying this population we can learn about the star formation history of the universe, and because the starbursting is triggered by merger events, we can also probe models of structure formation and halo dynamics through the ages.

Around 1 mm wavelengths it is possible to find similar starbursts across much of the volume of the universe, because the dimming of radiation from increasing distances is countered by the steeply rising energy spectrum between 2 mm and 200 μm in the rest frame. Thus, an IR galaxy would produce nearly the same (sub)millimeter flux regardless of its distance in the range of z ~ 0.5–10.

The nearly bias-free selection, together with the fundamental desire for studying starbursts, make submillimeter surveys (Coppin et al. 2006; Weiss et al. 2009; Austermann et al. 2010; Ivison et al. 2010) especially relevant. However, while finding submillimeter-selected galaxies (SMGs) is relatively straightforward, studying them in any detail has proved difficult. This is due to two factors: they are faint at other wavelengths, and there are often multiple possible optical/NIR counterparts (see Pope et al. 2006; Younger et al. 2009) due to the poor spatial resolution of most (sub)millimeter telescopes (typically 10”–30” FWHM).

As a result, most spectroscopic redshifts have been obtained for SMGs with radio-detected counterparts providing the required positional accuracy. Thus, Chapman et al. (2003, 2005) and Kovács et al. (2006) discovered that most SMGs lie around a median redshift of 2.3, are extraordinarily luminous (10^{12–10^{13}} L_⊙), and have large molecular gas reservoirs (10^{10–10^{11}} M_⊙). The close correlation between IR and radio luminosities of SMGs resembles that of local star-forming galaxies (Helou et al. 1985; Condon & Broderick 1991; Condon 1992; Yun et al. 2001), implying that star formation is the principal power source.

Despite these successes, however, the number of SMGs with spectroscopic redshifts is only around a hundred, and less than half of these are characterized in the far-infrared
Table 1

| Band/Instrument | Criterion |
|-----------------|-----------|
| IRAC            | $S_{3.6 \mu m} < S_{4.5 \mu m} < S_{5.8 \mu m} > S_{8.0 \mu m}$ |
| MIPS 24        | $S_{24 \mu m} > 400 \mu Jy$ |
| MAMBO           | $S_{1.2 mm} \gtrsim 2 \ mJy$ |

Note. Summary of the selection criteria for the MAMBO-detected 5.8 $\mu$m peak samples of L09 and F09.

1.1. SMGs and Spitzer

A major step forward in understanding SMGs was provided by Spitzer. With its sensitive mid-IR imaging and spectroscopic capabilities, Spitzer detected most SMGs in multiple mid-IR bands, which can provide accurate photometric redshifts $dz/(1 + z) \approx 0.1$ (Pope et al. 2006; Lonsdale et al. 2009). Furthermore, many Spitzer-selected objects are predicted to be submillimeter bright (Lonsdale et al. 2009, hereafter L09). Unfortunately, the identification of mid-IR counterparts to SMGs is plagued by problems similar to those of optical association (Pope et al. 2006), and so the reliance on radio associations remains.

Selecting strongly luminous starbursts at $z \sim 2$ from Spitzer data can overcome these problems, and the resulting samples are expected to contain a large proportion of SMGs within them. Thus, a two-step process has been suggested. First, selecting sources with peak Spitzer-Infrared Array Camera (IRAC) flux densities in the 5.8 $\mu$m channel should remove galaxies with a mid-IR luminous active galactic nucleus (AGN; Weedman et al. 2006; Farrah et al. 2008), leaving objects with a clear rest-frame 1.6 $\mu$m opacity minimum at $z \approx 2$. The required IRAC detections ensure that stellar masses are large, especially when applied to limited sensitivity samples such as SWIRE (Lonsdale et al. 2003). Second, a bright 24 $\mu$m flux density cut ($S_{24 \mu m} > 400 \mu Jy$) favors starbursts at the same redshift as the strong rest-frame 7.7 $\mu$m polycyclic aromatic hydrocarbon (PAH) emission feature is redshifted into the band. Redshifts from Infrared Spectrograph (IRS) spectra or from IRAC photometry confirm that most sources selected in this way lie at $z \approx 2$ (Weedman et al. 2006; N. Fiolet et al. 2010, in preparation). The effectiveness of such a two-pronged selection was confirmed by L09 and Fiolet et al. (2009), hereafter F09, who detected a significant fraction of these sources at 1.2 mm using the MAMBO camera at the IRAM 30 m telescope (i.e., $S_{1.2 mm} \gtrsim 2 \ mJy$). Clearly, the proposed Spitzer selection (see Table 1) yields distant luminous starburst galaxies without radio preselection.

A key question is to what extent the SWIRE-selected samples are in fact representative of the purely submillimeter-selected population. A straightforward way to test this is to constrain where the peak of the IR emission lies, thus bridging the gap between the cold dust detected by MAMBO, and the hot dust and PAHs detected by Spitzer. Such constraints can be used to derive effective dust temperatures and accurate IR luminosities, for comparison with the overall SMG population. Because the sample consists of galaxies at $z \sim 2$, and dust temperatures are expected in the range of 30–40 K, the 350 $\mu$m band offers an ideal opportunity for providing the constraints we seek.

For our study, we targeted 12 galaxies from F09 and another 8 from L09. The former is an almost complete sample of sources from 0.5 deg$^2$ satisfying the criteria of Table 1, whereas the L09 sources are drawn arbitrarily from $\sim 30$ deg$^2$. To enhance our chances of detection at 350 $\mu$m, we selected objects with clear MAMBO detections, with an additional preference toward the highest 1.2 mm flux density measurements.

The observations are described in Section 2 and the results are summarized in Section 3, where we also discuss one of the submillimeter sources, which appears to be a close association of several IR galaxies. In Section 4, we develop appropriate spectral energy distribution (SED) models to interpret the measurements. With these models, we characterize the sample in Section 5, deriving precise dust temperatures, dust/gas masses, and luminosities, and with them we verify the (far)infrared to radio correlation.

We assume a cosmology with $H_0 = 71 \ km \ s^{-1} \ Mpc^{-1}$, $\Omega_m = 0.27$, and $\Omega_L = 0.73$, and calculate distances as prescribed by Hogg (1999).

2. SHARC-2 350 $\mu$m OBSERVATIONS

350 $\mu$m observations were carried out at the 10.4 m Caltech Submillimeter Observatory (CSO), using the SHARC-2 Camera (Dowell et al. 2003). Data were collected during five successful observing runs between 2007 January and 2009 February. The typical weather conditions during observing ranged from good to marginally useful, with in-band line-of-sight opacities $\tau \approx 1–2$, corresponding to precipitable water vapor levels around 0.7–1.3 mm.

We took advantage of the open-loop actuated Dish Surface Optimization System (DSOS; Leong et al. 2006) of the telescope to maintain the optimal beam qualities at all elevations. As a result, we expect our telescope beam efficiencies to be relatively high and limited mainly by the 12 $\mu$m surface rms of the CSO panels.

Our observing strategy was to modulate the telescope primary with small, field-of-view-sized open Lissajous patterns (Kovács 2008b, 2006), with average scanning speeds around a beam per second. These patterns facilitate the separation of the astronomical source from the various correlated signals (of the atmosphere or the instrument). At the same time, the pattern provides uniform coverage over the field of view, the source remains exposed on the array at all times, and the scanning mode does not require extreme maneuverability of the telescope structure.

In total, we spent 37.5 hr on the 20 objects observed. We aimed for 5$\sigma$ detections, or limiting rms noise levels of 10–12 mJy beam$^{-1}$. Pointing and flux density calibration measurements were taken frequently, at least once per hour during the observing period. Our principal flux density calibrators were Mars, Arp 220 (9.93 ± 0.11 Jy, based on our own calibration against planets and asteroids), and the minor planets Ceres, Juno, and Vesta, for which appropriate temperature models have been derived by C. D. Dowell and are available through the SHARC-2 Web site. In addition, we relied on the evolved star CIT6 and the quasar 3C 273 as additional calibrators, owing to their relative proximity to the targeted fields in the Lockman Hole. To counter the long-term variability of CIT6 we measured it against our main calibrator sources during each observing run, while 3C 273 we cross-calibrated on a daily basis (see Table 2).

15 www.submm.caltech.edu/~sharc
pointing accuracy of the SHARC-2 data is expected at
of our sources due to systematic pointing errors, the pointing
variations tend to be greatest. To avoid the unnecessary smearing
targets.

Based on the residual scatter of calibrator flux densities, we ex-
pect a 350 $\mu$m calibration accuracy around 8% for our science
targets.

We checked and adjusted the focus settings several times
during each night, more frequently near sunrise and sunset when
variations tend to be greatest. To avoid the unnecessary smearing
of our sources due to systematic pointing errors, the pointing
data of each run were carefully analyzed for trends. Corrections
were applied as required at the time of reduction. The final
pointing accuracy of the SHARC-2 data is expected at $\simeq 3''$
rms.

We reduced the data using the CRUSH software (1.996
a5; Kovács 2008a, 2006), which estimates and removes the
correlated atmospheric and instrumental signals, solves for the
relative detector gains, and determines the appropriate noise
weighting of the time streams in an iterated pipeline scheme.
To maintain calibration accuracy, the inherent filtering of point-
source signals by the reduction steps is carefully estimated and
corrections are applied internally by CRUSH.

3. RESULTS

We detected all 20 of the targeted sources. In a few cases, the
detections are tentative. The measured 350 $\mu$m flux densities are
listed in Table 3, along with all prior measurements relevant to
this work. We reached rms sensitivities of $4-10$ mJy beam$^{-1}$
in all but one field. 80% of the 350 $\mu$m detections are robust (>4$\sigma$),
two are 3$\sigma$–4$\sigma$ and another two are marginal (<3$\sigma$). However,
even the lowest signal-to-noise detection is significant (with a
confidence level >95%) given the small, beam–sized search
areas surrounding the IRAC (and nearby radio) positions. For
the most part, the SHARC–2 positions are in excellent agreement
with those from IRAC, with deviations at $\lesssim 3''$ rms.

3.1. Submillimeter Multipliers

There is, however, the curious case of L–23 (see Figure 1),
with an elongated 5.7$\sigma$ SHARC–2 peak 13'5 from the IRAC
and radio positions. The discrepancy is too large (>4$\sigma$) to be a
statistical pointing error. Coincidentally, we have a large number of
pointing measurements both before and after observing
the galaxy in question, all reinforcing an absolute 350 $\mu$m
astrometric accuracy better than 3'' rms. Thus, the single

$\sigma$

Note. The columns are: the name of the variable calibrator source, the period of
measurements, the number of measurement, the derived 350 $\mu$m flux densities,
and the stable cross-calibrator sources used.

Note. Source IDs prefixed with LH or EN are from L09, whereas those lettered with L are from F09. SHARC–2 detection offsets are with respect to the
SWIRE catalog coordinates. 1.2 mm flux densities are from L09 and F09, 20 cm radio data from Owen & Morrison (2008), 50 cm value from F. Owen et al.
(2010, in preparation), while 90 cm points are from Owen et al. (2009). The quoted rms uncertainties do not include the uncertainties in the calibration.

a Photometric redshift from L09.

b IRS Spectroscopic redshift from L09.

c IRS Spectroscopic redshift from N. Fiolet et al. (2010, in preparation).

Photometric redshift from F09.

The 350 $\mu$m flux density of L–23 is from the undeconvolved image close to the
instrument resolution (middle panel of Figure 1).

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instrument resolution (middle panel of Figure 1).
MIPS and radio sources are discussed in Section 3.1.

22.5 mJy beam$^{-1}$ in the deconvolved flux densities we estimate at around 5 mJy. Positions are

The SWIRE $\mu$-peak is inconsistent with a source at the IRAC and SHARC-2 peak is inconsistent with a source at the IRAC and radio positions.

A substructure of the peak is revealed if we smooth less than the optimal amount for point-source extraction. We find a banana-shaped feature dominating the 350 $\mu$m emission to the east, and a fainter $\sim 2\sigma$ compact peak close to the expected position. The position and point-like nature of the fainter component is consistent with both our pointing accuracy, and the expected size ($\lesssim 1''$) of a galaxy at $z = 2.38$. Therefore, we identify this as the 350 $\mu$m counterpart to L-23.

Deconvolution of the elongated feature suggests three distinct components. Two of these align well with nearby IRAC and MIPS 24 $\mu$m peaks (at $10^4.47^{m}28^{s}1$, +58°52′20″ and $10^4.47^{m}28^{s}04$, +58°52′14″) and radio sources (10$^4.47^{m}28^{s}45$, +58°52′20″ and 10$^4.47^{m}27^{s}97$, +58°52′14″), while the third peak is perhaps a super-resolution artifact. The positions and approximate brightness of the deconvolved peaks are summarized in Table 4.

It is not unusual to find resolved pairs of submillimeter sources with $\sim 20''$–$30''$ separation (Blain et al. 2004; Greve et al. 2004; Farrah et al. 2006; Weiss et al. 2009). Such pairs are relatively infrequent and correspond to massive dark matter halos ($>10^{15} M_{\odot}$). However, the clustering of SMGs on smaller scales is not well constrained. Therefore, the blending of as many as three or four galaxies into a single 350 $\mu$m detection peak (with total $S_{350\mu m}$ $\approx$ 60 mJy) is interesting.

We often assume that each deep-field (sub)millimeter detection corresponds to just one luminous galaxy, with unique counterparts at optical, IR, or radio wavelength. Granted that the clustering of SMGs on scales $\lesssim 15''$ is not well known, it seems reasonable given the generally low density ($\sim 400/\text{deg}^2$) of sources in the current, shallow (sub)millimeter surveys. However, our multiplet puts this assumption to the test: the 350 $\mu$m components that we identify around L-23 would constitute a single source under the spatial resolution ($15''$–$30''$) of current (sub)millimeter surveys. The fact that it is a triplet or a quadruplet suggests that unresolved doublet, or even triplet (sub)millimeter sources may abound. The $\sim 20\%$ fraction of the radio-identified SMGs with multiple radio counterparts (Ivison et al. 2007) could be an indication of the frequency of unresolved (sub)millimeter multiplets, which is also consistent with Aravena et al. (2010). As such, the ubiquitous presumption that (sub)millimeter sources are individual galaxies may not be entirely justified.

If multiple luminous galaxies are often behind the low-resolution (sub)millimeter peaks, the implications would be wide ranging. Some or all of the IRAC sources commonly detected close to an uncertain (sub)millimeter position (e.g., Pope et al. 2006; Younger et al. 2009) could each contribute comparably to the measured (sub)millimeter flux densities. A commonality of multiplets would imply that (sub)millimeter source counts may be steeper than what SHADES (Coppin et al. 2006), AzTEC (Austermann et al. 2010), or the LABOCA deep-field survey (Weiss et al. 2009) found; by counting multiple faint sources as a single bright one, these surveys would slightly underestimate the abundance of faint galaxies while substantially overestimating the number of bright ones (i.e., ULIRGs and hyper-LIRGs). Submillimeter surveys by Herschel (especially at 250/500 $\mu$m) would be similarly affected. A strong clustering of SMGs at separation angles $\lesssim 20''$, i.e., below the smallest scales that current (sub)millimeter surveys can resolve, would be implied. Unresolved multiplets could partially explain why as many as half of the SMGs in the literature have no identifiable radio counterparts: as opposed to having one detectable counterpart, there may be a number of associated faint radio sources below the detection level.

4. SPECTRAL ENERGY DISTRIBUTIONS

The addition of the 350 $\mu$m data to the existing measurements provides a powerful constraint on the FIR SEDs of the SWIRE-selected samples of L09 and F09. It allows, for the first time, an accurate characterization of the dust temperatures through the effective dust temperature $T_{d}$.
and luminosities of individual sources in the sample, provided that physically realistic models of emission are fitted to the observations.

Before the emergence of details on the Wien-side shape of the SEDs (e.g., from Spitzer), it was common practice to rely on single-temperature dust models. Extra temperature components were added as necessary to fit data at wavelengths $\lesssim 100$ $\mu$m. However, such models were clearly very naive. Among the many more physically motivated treatments is the pioneering work by Désert et al. (1990) who considered dusty environments exposed to a range of radiation fields. Their framework has been fine-tuned to better match observations, especially of the aromatic index $\beta$, which is observed near $\nu_{\text{pk}}$. The spectral emissivity index $\beta$ can be related to the characteristic photon cross-section $\kappa_0$ to mass ratio of particles at $\nu_0$. The spectral emissivity index $\beta$ can be related to the fractal dimension $D$ of the dust particles as $\beta = D - 1$ (Yang 2007). Thus, $\beta$ values are expected in the range of 1–2, depending on the shape of particles. There have been several attempts for determining appropriate $\kappa$ values for interstellar dust particles (e.g., Hildebrand 1983; Krügel et al. 1990; Sodroski et al. 1997; James et al. 2002). The resulting scatter of values reflects the difficulty of making such measurements. In this work, we assume $\kappa_0$ = 0.15 $m^2$ kg$^{-1}$, which matches the value used by Kovács et al. (2006) and is based on an average 125 $\mu$m value (Dunne et al. 2003) assuming $\beta = 1.5$. As the strength of emission depends on the $\kappa_0 M_d$ product, the inherent uncertainties in $\kappa$ ultimately affect the accuracy to which dust masses can be determined. At the same time, the temperatures and luminosities can be determined accurately and independently from the assumptions on the absorption efficiency.

We can calculate single-temperature IR luminosities $L_\nu$ by integrating the de-magnified observed flux density at luminosity distance $D_L = D_A(1 + z)^2$ from the source:

$$L_\nu(T) = 4\pi D_L^2 m^{-1} \int_0^\infty S_\nu(v, T)dv.$$ 

The integration can be performed analytically in the optically thin limit ($\tau \ll 1$), giving

$$L_\nu(T) = \Gamma(4 + \beta)\tau(4 + \beta) \frac{8\pi h}{c^2} \left[ \frac{kT}{h} \right]^{4} A_{\text{eff}},$$

in terms of the effective surface area of emission $A_{\text{eff}}$, Planck’s constant $h$, the Boltzmann constant $k$, the speed of light $c$, and Riemann’s $\Gamma$ and $\zeta$ functions. The same expression is also applicable for the case of optically thick emission ($\tau \gg 1$) by setting $\beta = 0$. The effective area of emission $A_{\text{eff}}$, in the optically thin and thick limits, respectively, is given by

$$A_{\text{eff}} \approx \begin{cases} M_d \kappa_0 (kT/h\nu_0) & \text{if } \tau \ll 1, \\ d\Omega D_A^2 & \text{if } \tau \gg 1 \text{ or } \beta \to 0. \end{cases}$$

Given the relation of the projected surface area to total emitting area ($\pi r^2$ versus $4\pi r^2$ for a sphere), our expression for the optically thick limit recovers the Stefan–Boltzmann law of blackbody luminosities. In the optically thin limit, $A_{\text{eff}}$ is the physical emitting area at the frequency $\nu = kT/h$. From a computational point of view, it is practical to approximate the Riemann $\Gamma$ and $\zeta$ functions in Equation (3) for the range of typical $\beta$ values:

$$\Gamma(4 + \beta)\tau(4 + \beta) \approx 6.45 \exp(1.24\beta + 0.11\beta^2),$$

which is accurate to about a percent in the range $\beta \approx 0.2$.

Interstellar dust emission is mostly optically thin at FIR wavelengths ($\lambda > 100$ $\mu$m). Only the more extreme galaxies and quasars, or strongly lensed objects, concentrate dust to such an extent that optical depths can become significant over the bulk of the emission spectrum. This is a concern, given the extreme nature of our objects. We therefore would like to also consider the effect of intermediate optical depths in deriving accurate luminosity measures.

### 4.1. Intermediate Optical Depths

We can derive approximations for the integrated luminosity for the general case of non-negligible optical depths. Our approach is based on the observation that most of the luminosity is radiated at frequencies close to the gray-body SED peak (see Equation (1)), which is observed near

$$\nu_{\text{pk}} \approx (3 + \beta) \frac{kT_{\text{obs}}}{h}.$$ 

Around the peak, we can approximate the frequency dependence of the emissivity, i.e., $\epsilon = (1 - e^{-\tau})$, with a power law $\epsilon \approx \epsilon_{\text{pk}}(\nu/\nu_{\text{pk}})^{\beta_{\text{eff}}}$, where, by definition, an effective spectral index $\beta_{\text{eff}}$ can be calculated as

$$\beta_{\text{eff}} = \frac{\partial \log \epsilon}{\partial \log \nu} = \frac{\nu \partial \epsilon}{\epsilon \partial \nu}.$$
Substituting the optical depth from Equation (2) and evaluating at the peak $\tau_{pk}$, we arrive at

$$\beta_{eff} = \beta \frac{\tau_{pk}}{e^{\tau_{pk}} - 1}. \quad (8)$$

Thus, the frequency dependence of the emissivity near the peak of the emission can be characterized by an effective gray-body index $\beta_{eff}$. This means that we can rely on Equation (3) to provide an approximation to the luminosity function, simply by replacing $\beta$ with $\beta_{eff}$ above together with an effective emission area:

$$A_{eff} \approx \frac{(1 - e^{-\tau_{a}})d\Omega D_A^2}{(3 + \beta)^{\beta_{eff}}}. \quad (9)$$

It is possible to refine this approximation by seeking simultaneous solutions to Equations (6) and (8) with $\beta \rightarrow \beta_{eff}$ in Equations (6) and (9).

4.2. Power-law Temperature Distributions

Single-temperature models can be useful, especially for offering comparison to earlier studies that analyzed data in this way. However, it is clear that such models fall short on the Wien side of the thermal emission spectrum (dotted line in the left panel of Figure 2). Measurements at wavelengths shorter than the peak (typically $\lesssim 200 \mu m$) by IRAS, ISO, or Spitzer all indicate that flux densities fall far less dramatically than single-$T$ gray-body models imply. Temperature estimates are biased by the inclusion of data on the Wien side (at $\lesssim 200 \mu m$ in the rest frame), and luminosities are systematically underestimated. The errors can be significant depending on the actual spectral profile, and the data used for fitting. This is a concern, since the SHARC-2 $350 \mu m$ point translates to rest-frame wavelengths of $90–175 \mu m$ at redshifts $z \sim 1–3$.

For improving our models, we look for clues in the same local starbursts that yield the oft-used templates for the interpretation of Spitzer data (Berta 2005; Polletta et al. 2007). Based on these galaxies we find that a power-law distribution of temperature components ($dM_d/dT \propto T^{-\gamma}$), with a low-temperature cutoff at $T_c$, are in excellent agreement with measurements (Figure 2). At the same time, power-law distributions are easily justified in a physical context. The radiative-transfer models of Dale et al. (2001) and Dale & Helou (2002) are similarly conditioned on dust being distributed in a range of radiation fields $U$ as $dM_d/dU \propto U^{-\alpha}$. Their power-law index $\alpha$ is also the Wien-side spectral index and depends on the geometric configuration of dust clouds relative to the heating sources. Under the assumption of radiative dust heating the two models are approximately equivalent with $\gamma \approx 4 + \alpha + \beta_{eff}$. Therefore, we expect $\gamma \approx 6.5–7.5$ for sources embedded in a diffuse medium (e.g., star formation), and $\gamma \approx 4–5$ if absorption happens inside a dense medium at a well-defined distance from the source (e.g., for a molecular ring surrounding an AGN).

We argue that a temperature distribution (as opposed to a radiation-field distribution) offers a more general treatment, because it can also account for non-radiative heating of dust particles, e.g., by shocks or gravitational collapse. One needs only to remember that one of the critical functions of dust in star formation is to act as a coolant during the collapse of star-forming gas clouds. Thus, dust heating begins even before the UV-bright OB stars illuminate the interstellar medium. Temperature distributions can further arise from a distribution of individual molecular clouds in a galaxy, each with its own size and environment.

Apart from the physical plausibility of power laws, a practical advantage is that they add just a single variable $\gamma$ to the parameterization of single-$T$ models. This is welcome, especially since the number of SED measurements across the FIR band are...
generally few, even for many well-studied local galaxies, allowing robust constraining only for a handful of parameters.

We can write appropriate expressions for predicted flux densities in terms of the single-$T$ flux $S_1$ (Equation (1)) as

$$S_{\text{vobs}}(T_c) = (\gamma - 1)T_c^{-\gamma} \int_{T_c}^{\infty} S_1(\nu_{\text{obs}}, T_{\text{obs}}) T^{-\gamma} dT,$$

where once again $T_{\text{obs}} = T/(1 + z)$. The integration can be performed numerically with a number of discrete temperature components, or can be written in a closed form (see Köhler [1970]) using the incomplete Riemann zeta function $Z_\gamma(y - 1, \log \nu_r/kT_c)$ and $\Gamma(y - 1)$. Luminosities can be expressed in a closed form and are given by

$$L = \gamma - 1 \gamma T_{\text{obs}} \int_{T_c}^{\infty} S_1(\nu_{\text{obs}}, T_{\text{obs}}) T^{-\gamma} dT,$$

based on the single-$T$ value $L_1$ (Equation (3)). Finiteness of luminosities requires that $\gamma$ be larger than 5+$\beta$ eff.

Our measure of the luminosity accounts for the full power radiated through thermal dust emission, in contrast to a more traditionally defined FIR or IR luminosities, which measure output inside a strictly defined wavelength ranges (e.g., between 40 $\mu$m and 1000 $\mu$m). As such, our expression for the integrated luminosity can be applied to a wider range of environments (e.g., hot accretion disks) than definitions based on strict wavelength ranges. Additionally, $L$ provides a fair proxy for the total bolometric luminosity of warm ($\gtrsim 30$ K) LIRGs, where an overwhelming fraction of the total power output is absorbed and re-radiated by dust.

4.2.1. Clues from Local Starbursts

To check what $\beta$ and $\gamma$ describe the local starbursts best, we fitted a selection of published FIR continuum data uncontaminated by aromatic features or synchrotron emission, in the 6 $\mu$m–2 mm range, with power-law $T$ distributions and assuming

Table 5: FIR and Radio Properties of Local Starbursts

| Name          | $D_L$ (Mpc) | $N_{IR}$ | $N_{rad}$ | $|X_r|$ | $T_c$ (K) | $\gamma$ | $\log M_d$ ($M_\odot$) | $\log L$ ($L_\odot$) | $\tau_{\text{IR}}$ | $q$ | $\alpha$ |
|---------------|-------------|----------|-----------|--------|-----------|----------|----------------------|--------------------|-----------------|----|---------|
| Arp 220       | 77.6        | 15       | 7         | 0.92   | 36.4 ± 1.2 | 7.7(2)   | 7.9(3)               | 12.16(2)           | 0.68            | 2.47(4) | 0.25(4) |
| IRAS 20551-4250 | 188        | 10       | 1         | 0.99   | 37.9 ± 2.1 | 7.2(3)   | 7.3(3)               | 12.09(3)           | 0.19            | 2.61(9) | ...     |
| IRAS 22491-1808 | 348        | 14       | 1         | 0.68   | 39.0 ± 0.2  | 7.6(3)   | 7.6(2)               | 12.20(3)           | 0.38            | 2.91(7) | ...     |
| M 82          | 3.57        | 11       | 9         | 0.99   | 35.4 ± 2.0  | 7.1(3)   | 6.1(2)               | 10.86(2)           | 0.12            | 2.39(8) | 0.65(5) |
| NGC 6090      | 127         | 11       | 1         | 1.81   | 28.0 ± 1.9  | 6.9(3)   | 7.4(2)               | 11.67(2)           | 0.15            | 2.33(12) | ...     |
| NGC 6240      | 105         | 21       | 7         | 1.07   | 32.3 ± 1.1  | 7.1(1)   | 7.5(4)               | 11.96(2)           | 0.25            | 1.84(4) | 0.85(3) |

Notes: The FIR and radio properties of local starbursts, from the multi-$T$ fits to a selection of available IR continuum data in the 6 $\mu$m–2 mm range, with $\beta = 1.5$ and assuming typical emission diameter of 1 kpc (or 300 pc for M 82). The synchrotron component is modeled as a simple power-law $S_{\text{rad}} \propto v^{-\alpha}$. Columns are: the object name, luminosity distance $D_L$, the number of IR and radio density points ($N_{IR}$ and $N_{rad}$) used, the residual scatter $|X_r|$ around the fit, the temperature $T_c$ of the dominant cold component, the mass–temperature index $\gamma$, dust masses $M_d$, integrated IR luminosities $L$, the optical depth $\tau$ around the IR emission peak $\nu_{\text{peak}}$, and the radio–IR correlation constant $q$, and synchrotron spectral index $\alpha$. Uncertainties are the total errors, which are indicated in brackets for $\gamma$, $\log M_d$, $\log L$, $q$, and $\alpha$, and refer to the last digits in the quoted values. Dust masses assume $\kappa(850 \mu$m) = 0.15 $m^2$ kg$^{-1}$. Plots of these models and the data used for deriving them are available in the online edition.

In characterizing our SWIRE-selected samples, we assume $\beta = 1.5$ based on our findings on local starbursts and work by others. For the size of the emitting region (i.e., for setting $d\Sigma_d D_A^2$), we assume an average diameter of 3 kpc in our single-temperature fits. Such an extended starburst is unprecedented in the local universe, where the luminosities tend to originate from smaller kpc-scale molecular rings. Nevertheless, the larger sizes are reasonable for our sample (see, e.g., Farrah et al. 2008), where luminosities exceed the local examples by 1 or 2 orders of magnitude. The assumption on the extent of emission is critical only for interpreting the temperature parameter of the fit as a true measure of physical temperatures. The best-fit temperature values would rise if smaller emission diameters were assumed. At the same time, dust masses and integrated luminosities remain nearly independent of the size assumption, and thus offer robust characterizations. The resulting single-temperature fits to the sample are summarized in Table 6.
The FIR properties derived from the single-$T$ fits are based on the MAMBO 1.2 mm measurement and our SHARC-2 350 μm data only. Shorter wavelength data (especially MIPS 24 μm) were not included in these fits because these trace higher-temperature components and aromatic features, neither of which are accounted for in the single-$T$ dust model. We also do not include the 160 μm datum of EN1-04 for any of our modeling, because we find it to be inconsistent with the measurements at 24 μm and at 1.2 mm. We suspect that the uniquely detected 160 μm flux density of our sample may be contaminated by an unknown source close to EN1-04.

Even with all the caution we can summon, single-temperature models cannot yield accurate characterizations for reasons already dissected. We include these simple models only to provide a comparison to other studies (especially Kovács et al. 2006), which analyze FIR and (sub)millimeter data in this way. Fitting a distribution of dust temperatures to the data yields more realistic estimates of the dust masses and luminosities. Our best estimates of the underlying FIR properties are summarized in Table 7, and shown in Figure 2. The temperature parameter $T_c$ indicates the temperatures of the dominant coldest component, above which warmer components exist in lesser quantities (see Section 4.2). Therefore, it is not surprising that single-component fits, which measure an average temperature, should yield characteristic values above the cold cutoff temperatures $T_c$ in a distribution.

For our temperature-distribution fits, we have included the MIPS 24 μm data as guiding constraints on the short-wavelength tails of the dust continuum. It is clear, however, that the 24 μm flux density is likely dominated by emission from aromatic features. However, warm dust and PAH likely cohabit the same interstellar environments. Thus, PAH emission is almost certainly coupled to a comparably bright dust continuum. Consequently, one should anticipate close to constant PAH-to-continuum flux ratios for a class of star formation dominated objects. Based on the stacked IRS spectra of L09 we can estimate the typical continuum contribution to the MIPS 24 μm measurement as a function of redshift (Figure 3), with which we set appropriate 24 μm constraints for our fits. Recognizing, however, that the continuum fraction may vary significantly from one galaxy to the next, we assign an uncertainty of 0.25 dex to these 24 μm guestimates. Thus, we allow the 24 μm continuum fraction to span a full decade in brightness before the deviation becomes significant (i.e., $>\sigma$), while we assume that the average IRS spectrum of L09 is representative of the sample as a whole.

5. DISCUSSION

Under the assumption of extended starbursts we find that our models deviate from the optically thin limit only moderately, with $\tau \approx 0.7 \pm 0.2$ near the emission peaks (under the assumed emission diameters of 3 kpc). This is good news for a straightforward comparison to the SMGs of Kovács et al. (2006), which were analyzed under the optically thin assumption. These optical depths are not much higher than the opacities of local starbursts on kpc scales. We may take this as a first indication that our guess on the extent of star formation is correct.

The median 70 μm and 160 μm flux densities of 2.56 ± 0.38 mJy and 14.63 ± 4.05 mJy, respectively, from the stacked images of the MAMBO-detected sources of F09 agree well with the multi-$T$ models of our sources with median properties (i.e., $T_c = 33.5$ K, $M_d = 10^{8.82} M_\odot$ at $z = 2.05$), within the expected measurement uncertainties (see Figure 2). These prove the general reliability of the 24 μm continuum contribution estimates.

The use of the scaled 24 μm data further allows us to probe the range of $\alpha$ values and typical emission scales that are consistent with measurements. Accordingly, we find $\alpha = 6.71 \pm 0.11$ and average emission diameters around $\approx 2$ kpc fit the data.
best globally. We can exclude diameters <1.2 kpc with 95% confidence. Thus, we see our size assumption for the single-
diameter of 2 kpc in our multi-
likely. We can exclude diameters < 40% (i.e., 0.15 dex) measurement error, revealing only a hint of
an underlying scatter ≲20%. Assuming SMG-like gas-to-dust mass ratios of 54 (Kovács et al. 2006), which are also typical
from distinct compact nuclei separated at the inferred distance (e.g., in a merging system), whereas the best-fit SEDs are only
consistent with extended dust emission. The implied scales, spanning kiloparsecs across, are in line with Farrah et al. (2008)
and are a strong indication that dust heating is distributed, which in turn supports star formation as the primary power source.

Notes. A comparison of our Spitzer-selected samples to the local starbursts, and the classical SMGs of Kovács et al. (2006). Indicated are the ensemble average values and 1σ intrinsic scatters for the characteristic dust temperature (i.e., single-T temperature) $T_1$, cold-component temperature $T_c$, single-T dust mass $M_d$, single-T luminosity $L_1$, total (IR) luminosity $L$, the (F)IR-radio correlation measure $q$, and the characteristic opacity $\tau_{pk}$ near the peak of the emission. Only mean values are shown, when the intrinsic scatters are not detected. The last column shows the average mass–temperature distribution index $\gamma$ and its rms uncertainty. The dust masses assume $\kappa(850 \mu m) = 0.15 \text{ m}^2 \text{ kg}^{-1}$.

a These are the local starbursts of Table 5, which provide the SWIRE starburst templates (Berta 2005; Polletta et al. 2007).
b Based on our own multi-T fits to the Kovács et al. (2006) data and assuming $\gamma = 6.7$.

### Table 8

Comparison to Classical SMGs

| Sample          | $T_1$ (K) | $T_c$ (K) | $\log M_1$ | $\log M_d$ | $\log L_1$ | $\log L$ | $q$ | $\tau_{pk}$ | $\gamma$ |
|-----------------|----------|----------|------------|------------|------------|----------|-----|-------------|----------|
| Local starbursts | ...      | 34.7 ± 3.6 | ...        | 8.83       | 7.33 ± 0.62 | ...      | 12.59 ± 0.28 | 1.4 ± 0.5 | 2.0 ± 0.16 | 1.1 ± 0.2 |
| L09             | 36.1 ± 5.8 | 34.4 ± 4.2 | 8.96 ± 0.18 | 8.85 ± 0.12 | 12.59 ± 0.28 | 12.97 ± 0.22 | 12.54 | 12.91 | 2.08 ± 0.16 | 1.1 ± 0.2 |
| F09             | 36.5      | 33.1     | 8.83       | 8.80       | 12.54       | 12.93 ± 0.12 | 1.2 ± 0.4 | 6.71 ± 0.11 |
| L09 + F09       | 35.5 ± 2.2 | 33.5 ± 2.1 | 8.90 ± 0.07 | 8.82       | 12.56 ± 0.05 | 12.76 ± 0.61 | 2.12 ± 0.12 | 1.2 ± 0.5 | ... |
| SMGs            | 34.1 ± 9.5 | (30.4 ± 8.5)$^b$ | 8.96 ± 0.32 | (8.85 ± 0.18)$^b$ | 12.60 ± 0.48 | (12.76 ± 0.61)$^b$ | 2.12 ± 0.12 | (1.2 ± 0.5)$^b$ | ... |
| SMGs(1 < z < 2.5) | 32.1 ± 5.6 | (30.8 ± 5.5)$^b$ | 9.07 ± 0.26 | (8.87 ± 0.11)$^b$ | 12.57 ± 0.30 | (12.82 ± 0.35)$^b$ | 2.05 ± 0.21 | (1.2 ± 0.4)$^b$ | ... |

For star-forming galaxies, we expect $\gamma \approx 6.5 + \beta_{eff}$ based on Dale et al. (2001). With $\tau_{pk} > 1.2 \pm 0.4$ near the emission peaks (corresponding to the most likely emission diameters of 2 kpc), it is not surprising that the SWIRE-selected sample has $\gamma$ values below those of local starbursts. The relatively shallow temperature distributions in turn might explain the unusually high 24 μm to 1.2 mm flux density ratios reported by L09 and F09. The implied radiation-field distribution indices $\alpha > 2.0$–2.35 further support star formation as the primary heating source behind the extreme luminosities.

![Figure 3](image-url) Expected continuum contribution to the MIPS 24 μm measurements. The top panel shows the average IRS spectra of eight L09 sources (thin solid line), and as it would appear under the resolution of the MIPS 24 μm band (thick solid curve). Based on the decomposition of this spectrum into starburst PAH features (NGC3079) and a power-law continuum (dashed line) contribution $\propto \lambda^{-\beta}$ (see L09), we estimate the typical continuum contributions to the MIPS 24 μm flux as a function of redshift (bottom panel) for the SWIRE-selected samples of L09 and F09, which we use to derive appropriate continuum constraints at 24 μm for our SED fits.

![Figure 4](image-url) Radio to (far-)infrared correlation. We plot the $q$ values for our sample, computed according to Equation (12) using the luminosities from Table 7 and $v_n = 9$ THz. Also shown are the best-fit ensemble average value of 2.08 ± 0.04 (solid line with shaded band), and the estimated 2σ underlying scatter of data around it (dotted lines).

(A color version of this figure is available in the online journal.)
product of our selection criteria, which favor objects close to $z \approx 2$. Since the radio co-selected SMG population peaks around $z \approx 2.3$ (Chapman et al. 2003, 2005), we conclude that two-pronged SWIRE selection (seeking the 24 $\mu$m bright population of 5.8 $\mu$m peaks) is effective in identifying a representative subset of SMGs at mid-IR wavelengths.

5.1. Radio–FIR Correlation

Our dust fits point to a tight correlation between IR and radio luminosities. This is witnessed by the consistent $q$ values in Tables 6 and 7, which were calculated according to Equation (12). Such correlations are well known for various local galaxies (e.g., Helou et al. 1988; Condon & Broderick 1991; Condon 1992; Yun et al. 2001), and extend to various populations into the distant universe (see Garrett 2002; Appleton et al. 2004; Beelen et al. 2006; Kovác et al. 2006). A flux density-based measure of the correlation was originally formulated by Helou et al. (1985) using 1.4 GHz radio and IRAS 60 $\mu$m and 100 $\mu$m flux densities. However, since we do not have the data in the rest-frame IRAS bands to use with the original definition, we can either guess these from our models, or redefine the correlation in terms of the quantities we can measure more directly.

The existence of the correlation is not surprising as both the synchrotron emission and the IR luminosities are driven by the short-lived population of high-mass ($\gtrsim 8 M_\odot$) stars. The synchrotron emission arises when relativistic electrons, which are produced by supernovae, decelerate in the magnetic fields of galaxies. At the same time, the IR heating is dominated by the luminosities of massive OB stars. With short-lived massive stars responsible for both, measures based on luminosities, not flux densities, are expected to capture the essence of the correlation more accurately. Unlike many prior studies of the correlation, we have the advantage of well-constrained, precise luminosity estimates. Accordingly, we can express the logarithmic correlation constant as

$$q = \log \left( \frac{L}{\nu_n L_{1.4 \text{GHz}}} \right), \quad (12)$$

with an appropriately chosen normalization frequency $\nu_n$ for the IR luminosity. The rest-frame radio luminosity density $L_{1.4 \text{GHz}}$ is calculated from the observed flux density $S_{1.4 \text{GHz}}$ using

$$L_{1.4 \text{GHz}} = 4\pi D_L^2 (1+z)^{1-\alpha} S_{1.4 \text{GHz}} \quad (13)$$

in terms of the luminosity distance $D_L$ and radio spectral index $\alpha$. The analysis of the SWIRE/MAMBO sample uses $\alpha$ values quoted in F09, while for the local starbursts we fitted $\alpha$ along with the other parameters.

It is practical to choose the normalization frequency $\nu_n$ such that the resulting $q$ values can be compared directly to the widely used original measure of Helou et al. (1985), which assumed typical temperatures of 40 K. We pick $\nu_n$ such that the definitions match exactly at that temperature, giving $\nu_n \rightarrow 4.52$ THz used with $L_1$ (see Kovác et al. 2006), or $\nu_n \rightarrow 9.0$ THz used with $L$ assuming $\gamma = 7.2$. Consequently, our $q$ values closely mimic the Helou et al. (1985) definition. The correlation measures $q$ for our single- and multi-temperature fits are listed in Tables 6 and 7, respectively.

A different definition was suggested recently by Ivison et al. (2010), who normalize IR luminosities, measured in the 8–1000 $\mu$m band, with $\nu_n = 3.75$ THz intended for the 40–120 $\mu$m band by Helou et al. (1985). Their measure no longer offers a direct comparison to many earlier studies, which is why we prefer ours. However, our $q$ values can be compared to Ivison et al. (2010) after adding 0.38 (i.e., $\log(9.0/3.75)$).

We find best-fit average $q$ values of $2.11 \pm 0.08$ with the single-temperature dust models and $2.08 \pm 0.04$ for the power-law temperature distributions. The implied intrinsic scatters, over the measurement uncertainties, are estimated at 0.18 and 0.16, respectively. Both our mean values and intrinsic scatters (Figure 4) are significantly below those in local studies, and comparable to the SMGs analyzed by Kovács et al. (2006), and to the $q_{\text{IR}} \sim 2.40$ found by Ivison et al. (2010) for their correlation measure. The result further supports the conclusion that our sample primarily consists of classical SMGs, without significant excess heating either by an AGN, or by low-mass stellar populations (which are likely partially responsible for the higher average $q$ values observed in the local universe).

6. CONCLUSIONS

Our main conclusion is that the mid-IR selection criteria of the L09 and F09, picking the bright 24 $\mu$m sources that are also 5.8 $\mu$m peaks, is effective in identifying a significant fraction of the SMGs around $z \approx 2$, thus providing a means of enhancing our understanding of the elusive SMG population through studies at mid-IR and shorter wavelengths. The FIR characteristics (dust masses, temperatures, and IR luminosities) of the SWIRE-selected sources are essentially identical to those of the classical SMGs at the same redshift. Additionally, the SWIRE-selected sample exhibits a correlation between radio and IR luminosities that is indistinguishable from that seen for SMGs. Our other conclusions are as follows.

1. To provide realistic FIR characterizations for the sample, we developed new models for the SEDs of galaxies with power-law mass distributions of temperature components. We demonstrated that such models describe local starbursts extremely well, under a tightly constrained dust emissivity index $\beta \approx 1.5$ and mass–temperature index $\gamma \approx 7.2$. The $\gamma$ values are consistent with what we expect for heating dominated by star formation.

2. We find that the most likely IR spectral continuum shapes of the distant SWIRE-selected starbursts differ only slightly from the local examples, with best-fit $\gamma \approx 6.7 \pm 0.1$. The lower $\gamma$ values are consistent with star formation under the high optical depths ($\tau_{90K} \approx 1.2$) in our sample.

3. Relying on the stacked IRS spectra of L09 for estimating the 24 $\mu$m continuum contribution, we place the typical diameter of starburst activity in these SMGs above 1.2 kpc (with 95% confidence), and find a most likely value of 2 kpc.

4. The emission scales, the typical $\gamma$, and the consistently low $q$ values all confirm that star formation is the main power source in the galaxies of the sample.

5. One of our targets shows a close clustering of three or four 350 $\mu$m components, each of which contributes comparably to the observable 350 $\mu$m flux density under the 15″–30″ resolution of most current (sub)millimeter surveys. A commonality of unresolved SMG multiplets could bias our understanding of this population. We need further studies to explore the importance of close multiplets in current and future submillimeter surveys.

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