Circular Dichroism in Atomic Resonance-Enhanced Few-Photon Ionization

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We investigate few-photon ionization of lithium atoms prepared in the polarized 2p (\(m_\ell = +1\)) state when subjected to femtosecond light pulses with left- or right-handed circular polarization at wavelengths between 665 nm and 920 nm. We consider whether ionization proceeds more favorably for the electric field co- or counter-rotating with the initial electronic current density. Strong asymmetries are found and quantitatively analyzed in terms of “circular dichroism” (CD). While the intensity dependence of the measured CD values is rather weak throughout the investigated regime, a very strong sensitivity on the center wavelength of the incoming radiation is observed. While the co-rotating situation overall prevails, the counter-rotating geometry is strongly favored around 800 nm due to the 2p-3s resonant transition, which can only be driven by counter-rotating fields. The observed features provide insights into the helicity dependence of light-atom interactions, and on the possible control of electron emission in atomic few-photon ionization by polarization-selective resonance enhancement.

I. INTRODUCTION

The response of matter to circularly polarized light can depend on the helicity of the light’s polarization. This phenomenon is referred to as circular dichroism (CD) and is widely exploited, e.g., in the analysis of chiral molecules (see Ref. [1] for an overview). Biomolecules, such as sugar or amino acids, are prominent examples of chiral targets for which single- [2–4] and multi-photon ionization [5–7], as well as tunnel ionization in intense laser fields [8], exhibit a dependence on the light’s helicity even for randomly oriented molecules. These dichroic differences have even been suggested to be the symmetry-breaking cause of life’s homochirality [9, 10]. Nevertheless, these effects are typically weak and vanish completely in the electric dipole approximation after integration over all possible target orientations.

For spatially aligned systems, in contrast, a CD signal occurs already for electric dipole transitions, resulting in much stronger asymmetries [11]. The most fundamental realizations of such oriented targets are polarized atoms with a magnetic quantum number \(m \neq 0\). In this situation, the helicity dependence is a result of either equal or opposite rotations of the electric field with respect to the initial current density of the active electron. Due to their fundamental importance, these benchmark systems have recently attracted considerable interest [12–19] in the study of the interaction between handed light and handed matter.

Atomic circular dichroism is quantitatively defined as

\[
CD = \frac{P_+ - P_-}{P_+ + P_-},
\]

where \(P_+\) and \(P_-\) are the cross sections for the co- and counter-rotating light polarizations respectively. In previous studies, it was found that there is no unambiguous answer to the fundamental question whether ionization proceeds more likely for the co- or the counter-rotating case. In the simplest case of one-photon ionization by a weak field, this question was already answered by Bethe and Salpeter, whose theoretical framework [20] delivers a CD value of close to 1, meaning that the co-rotating geometry is strongly favored [12, 21]. To the contrary, in the nonadiabatic tunneling regime, i.e., for intense fields, the ionization cross section was found to be larger for a counter-rotating field, thus leading to negative CD values.

In multi-photon ionization, the sign of the CD value features a dependence on the intensity of the ionizing field [17, 22]. This intensity dependence can be rather strong [18] due to “Freeman” resonances [23], where transient resonance enhancement occurs due to AC Stark shifts of intermediate levels.

In a recent Letter [19], two-photon ionization of polarized atoms was investigated in the case where resonance enhancement did not significantly affect the ionization rates. Lithium atoms were prepared in the 2p (|\(m_\ell| = 1\)) state and then ionized by a field (671 nm) tuned to the 2s – 2p resonance transition. A positive and weakly intensity-dependent value of the CD was found throughout the investigated intensity regime, while strong helicity-selective Autler-Townes shifts were observed for the counter-rotating geometry due to the coupling of the excited initial target state with its ground state. This peculiar feature allowed us to control not only the ionization probability, but also the photoelectron energy via the field polarization and intensity.

In the present study, we report an extension of our earlier work [19], now altering not only the intensity, but also the wavelength of the ionizing field. Specifically, we scan a wavelength range around the 2p-3s transition (at about 812 nm). Close to this resonance, the 2p state is ionized by the absorption of three photons, and resonance enhancement through the 3s state, as well as Autler-Townes
shifts due to the 2p–3s coupling, are expected to occur only for the counter-rotating geometry. In combination with the results reported in [19], the present work aims to understand the role of resonance enhancement in circular dichroism and the sensitivity of dichroic asymmetries to wavelength change of the ionizing radiation.

The experimental results are compared with theoretical predictions obtained by solving the time-dependent Schrödinger equation (TDSE). These results exhibit overall good agreement with the measured CD values. As in our earlier study, the present system represents a fundamental realization of a chiral system and, therefore, provides fundamental insights into implications of asymmetries in light-matter interaction.

II. EXPERIMENTAL SETUP

Our experiment was performed with the same apparatus described in [19]. It consists of three components: An all-optical lithium atom trap (AOT) [24], a tunable femtosecond light source, and a reaction microscope that allows us to measure the electron and recoil ion momenta after an ionization process [25, 26].

In the AOT, lithium atoms are laser-cooled to a temperature of about 1 mK in the field of continuous-wave laser beams near the 2s-2p resonance at 671 nm and trapped in a volume of approximately 1 mm diameter. In steady state, about 25% of the atoms in the trap are in the excited 2p state. A fraction of about 93% of these atoms are in a single magnetic sublevel with |m_e| = 1 with respect to the direction of a weak homogeneous magnetic field (about 5 Gauss), which is referred to as the z direction below. As detailed in [24], this high degree of polarization is achieved by an appropriate choice of the frequency as well as the polarizations of the cooling laser beams exploiting the Zeeman splitting of the magnetic sublevels as well as the dipole selection rules, respectively. This way an optical-pumping scheme is employed resulting in an average increase of the magnetic quantum number for each absorbed photon.

The femtosecond laser is based on a Ti:Sa oscillator with two noncollinear optical parametric amplifier (NOPA) stages similar to the setup reported in [27]. The oscillator provides pulses with wavelengths ranging from 660 nm to about 1000 nm with a pulse duration of 5 fs, a repetition rate of 80 MHz, and an average power of 200 mW. These pulses are stretched by passing through a combination of sapphire and fused silica windows to a duration in the order of about 1 ps. These strongly chirped pulses are superposed with a synchronized pump beam in two NOPA stages. The pump beam operates at a wavelength of 515 nm with a rate and duration of 200 kHz and 250 fs, respectively. Changing the relative timing between the pump pulse and the chirped oscillator pulse allows us to control the part of the spectrum that is amplified in the NOPA stages. In this way, the center wavelength can be tuned over the full wavelength range of the oscillator. Behind the NOPA stages, the pulses are recompressed by a set of chirped mirrors to a pulse length of several tens of fs. The laser is guided through the vacuum chamber at a small angle (10°) with respect to the z direction and focused on the target cloud with a beam waist of 50 µm. Peak laser intensities of up to \( I = 1.3 \times 10^{12} \) W/cm² were reached. Two typical spectra for center wavelengths of 670 nm and 790 nm are shown in Fig. 1.

The electron and ion momentum spectrometers are described in more detail in [25]. Briefly, electrons and target ions are extracted in opposite directions along the z axis by weak homogeneous electric and magnetic fields and detected with position- and time-sensitive microchannel plate detectors. The particles’ positions and time-of-flights allow us to determine their initial momenta [28, 29]. As mentioned above, the target cloud contains atoms in the 2s ground state and the excited 2p state. In order to separate the cross sections for the two initial states, the cooling lasers were switched off for 1 µs during every other femtosecond laser pulse. On the one hand, this switch-off duration is much longer than the lifetime of the excited 2p state (27 ns). Therefore, the spectra measured for the cooling lasers being switched off correspond to pure ground-state (2s) ionization. On the other hand, the switch-off duration is much shorter than typical timescales of the thermal motion (\( v \sim 1 \mu m/\mu s \)) of the atoms in the AOT. Therefore, the number density of the target atoms does not change significantly during the switching cycle, and the cross sections for the 2p initial state can be calculated by subtracting the 2s cross sections from the spectra measured for the cooling lasers being switched on by using an appropriate scaling factor that only depends on the previously determined fraction of atoms being in the excited state. Notably, knowing the excited population fraction allows also to cross-normalize
the cross sections for the two initial states.

Typical electron momentum distributions integrated in the z direction are shown in Fig. 2 for 2s ionization and 2p ionization with co- and counter-rotating helicities. In the present experiment, a resolution of 0.01 a.u. in the direction perpendicular to the femtosecond laser beam and of 0.005 a.u. in the direction longitudinal to it was achieved. For ionization with light of circular polarization in the xy plane, the momentum distributions shown in the figure should feature circular symmetry. However, in the experiment an enhancement in two opposite directions is observed. This is caused by the imperfect polarization of both the target atoms as well as the laser radiation, which is estimated to have an ellipticity of about 20%.

III. THEORETICAL MODEL

The experimental efforts are supported by ab initio calculations based on solving the time-dependent Schrödinger equation (TDSE) in the single-active electron (SAE) picture for a (nℓ) active electron in a He-like 1s2 ion core. Details of the potential, which is based on the static Hartree potential [30, 31] supplemented by phenomenological terms, are given in [19]. We achieved an accuracy of better than 1 meV for the n = 2 and n = 3 ionization potentials (IPs). The initial state of the TDSE is propagated in the velocity gauge, and the ionization probability is computed by projecting the time-dependent wavefunction at the end of the pulse onto scattering states. The earlier TDSE results exhibited excellent agreement with our experimental data for the photoelectron spectra and momenta measured under similar experimental conditions [19].

IV. RESULTS AND DISCUSSION

For the laser wavelengths and intensities investigated in this study, the Keldysh parameter γ for the valence ionization of lithium is always much larger than unity, such that the process can be described in the multi-photon picture in lowest-order perturbation theory (LOPT) [32]. Here, the absorption of one photon of right-handed circular polarization propagating along the quantization direction (i.e. the z direction) results in a change of the magnetic quantum number ∆m = +1, while the absorption of a left-handed circularly polarized photon leads to ∆m = −1. The resulting pathways for the three-photon ionization of Li (2p, m = +1) by co- and counter-rotating fields (λ = 795 nm) are depicted in Fig. 3 as red and blue arrows, respectively. There is only a single possible pathway for co-rotating ionization with the electron being promoted to a final continuum state with (ℓ, m) = (4, 4). For the counter-rotating case, in contrast, the final state is a superposition of (2, −2) and (4, −2) partial waves, respectively. Around a wavelength of 812 nm (neglecting the dressing of the states in the field), resonance enhancement is expected for counter-rotating polarization due to the presence of the 3s state. Two-photon resonances contribute, for either polarization, via the n = 5 levels at about 826 nm-829 nm, n = 6 at about 790 nm, n = 7 at 760 nm, n = 8 at 744 nm, etc.. The two-photon ionization threshold is reached at 700 nm. For 4-photon ionization of Li(2s) (dashed red arrows in Fig. 3), the final angular-momentum state is, respectively, (ℓ, m) = (4, −4) or (4, 4) for left or right-handed circular polarizations, resulting in identical cross sections for the two light helicities.

Different angular momenta contribute to the photoelectron angular distributions (PADs). The expected intensity distributions for the individual partial waves (ℓ, m) = (4, 4), (2, −2), and (4, −2) are shown in the top left panel of Fig. 4 as a function of the polar angle θ. For (ℓ, m) = (4, 4), the θ dependence is given by a sin^4(θ)-function with a narrow peak perpendicular to the quantization axis. A similar behavior is observed for (ℓ, m) = (2, −2) with a slightly broader peak following a sin^4(θ)-distribution. The g state with m = −2, in con-
FIG. 4. Photoelectron angular distributions for ionization by a laser field with a center wavelength of 795 nm and a peak intensity of $0.8 \times 10^{12}$ W/cm$^2$. Top left: $\vartheta$ distribution of partial waves corresponding to the spherical harmonics $Y_4^0$ (dashed red), $Y_2^{-2}$ (dotted blue), and $Y_2^{2}$ (solid black). Bottom left: Measured $\vartheta$ distribution for 2s ionization for left-(blue open triangles) and right-handed (green solid triangles) circularly polarized light along with the distribution of the partial wave with $(\ell, m) = (4, 4)$ (dashed red line). Right: Measured $\vartheta$ distribution for 2p ionization for co- (black solid squares) and counter-rotating (red open circles) cases with the partial waves $(\ell, m) = (4, 4)$ (dashed red line) and $(2, -2)$ (solid black line).

Contrast, features intensity not only at 90° but also at 40° and 140° with respect to the laser beam direction.

The comparisons to the experimental data for a center wavelength of 795 nm are shown in the two other panels of Fig. 4. As expected, the experimental electron angular distributions for 2s ionization are very well described by the $\sin^2$-distribution of a $g$ state (bottom left in the figure) for both helicities. The same behavior is observed for 2p ionization in the co-rotating geometry (Fig. 4, right). For the counter-rotating scheme, the $\vartheta$ dependence matches well with the $\sin^2$-distribution of the $d$ state. Notably, the cross section is rather small at angles where the $(\ell, m) = (4, -2)$ partial wave has its highest intensities, indicating that the final state is vastly dominated by the $\ell = 2$ wave. Qualitatively, the dominance of this $d$ state can be explained by ionization enhancement through the 2p-3s resonance, because in LOPT this pathway necessarily results in final $\ell = 2$ states. At other wavelengths, and in absence of the 2p-3s resonance, the angular distribution can be vastly different (see e.g. [19]).

Figure 5 depicts electron energy distributions for a laser wavelength of 795 nm with intensities of $0.8 \times 10^{12}$ W/cm$^2$ and $1.3 \times 10^{12}$ W/cm$^2$. For 2s ionization, the spectra exhibit a single peak around 0.9 eV. For 2p ionization, the peak is at slightly higher energies around 1.1 eV. These values agree with the expectations for four- and three-photon ionization of the two respective initial states. In our earlier experiment studying the ionization of the same atomic system at a shorter wave-length close to the 2s-2p resonance [19], intensity- and helicity-dependent photoelectron energy shifts of up to 40% were observed and explained by the Autler-Townes effect, which can be very strong in the vicinity of resonances. In the present case, such energy shifts are substantially smaller due to the much larger detuning of the laser center wavelength with respect to the resonance ($\Delta \lambda \approx 20$ nm as compared to 5 nm in the previous study) and the lower spectral density of the radiation (cf. Fig. 1).

The energy spectra shown in Fig. 5 are cross-normalized for the two laser field helicities exploiting the fact that the ionization cross sections for the spherically symmetric 2s initial state should be identical for both handesnnesses of the light. As can be seen from the figure, the ionization of the 2p state is strongly favored for the counter-rotating geometry. Using Eq. (1), this helicity dependence can be quantified. Negative $CD$ values of about $-0.49 \pm 0.1$ and $-0.54 \pm 0.1$, respectively, are obtained for both intensities. The error provided here is an estimate considering the statistical error as well as the uncertainty in the excitation ratio of the atoms in the AOT, which is about 25 ± 3%. Additional systematic uncertainties arise due to the imperfect polarization of both the laser radiation and the target atoms, as well as small drifts in the wavelength and intensity of the laser pulses during the measurements.

The intensity dependence of the $CD$ values was investigated in a series of measurements between $0.5 \times 10^{12}$ W/cm$^2$ and $1.3 \times 10^{12}$ W/cm$^2$ at a wavelength of $\lambda = 795$ nm. The obtained data are plotted in Fig. 6 (left) along with the values measured in our earlier experiment at $\lambda = 665$ nm, which are (partly) published in [19, 33]. For both wavelengths, the intensity dependence
is fairly weak. It should be noted that it is not possible to measure the cross sections at a single intensity in our experiment due to the spatial extension of the reaction volume and the intensity distribution around the focal point of the laser beam. The intensities given in the graphs correspond to their highest values while the measured data represent averages over the intensity distribution in the focal volume [34]. Notably, the CD values have opposite sign for the two wavelengths. As mentioned above, the difference can be explained by the 2p-3s resonance that enhances the ionization rate for the counter-rotating case around 815 nm.

The above observation suggests that, in the intensity and wavelength regime considered, the dependence of the CD on the wavelength of the incoming field is much stronger than its dependence on intensity. To obtain further insight, we varied the wavelength of the laser field between 740 nm and 795 nm at a constant intensity of about $5 \times 10^{11}$ W/cm$^2$ and measured the corresponding CD values. In this region, the CD monotonically drops from positive to negative values (see Fig. 6). When further measurements at higher and lower wavelengths with slightly different spectral widths and intensities were performed, a local minimum of the CD was observed at the 2p-3s resonance.

The measured CD values were compared with the results from the TDSE calculations. We used 35 fs FWHM (corresponding to a bandwidth of about 60 meV) Fourier-limited pulses with Gaussian envelopes and a peak intensity of $0.3 \times 10^{12}$ W/cm$^2$. We observe an overall good agreement between the measurements and the calculations (see Fig. 6). Note that the negative CD value around 800 nm is well reproduced theoretically. The calculation even predicts a second minimum with a negative CD value near 880 nm. However, no experimental data are available at this wavelength.

To obtain a better understanding of the alternating behavior of the CD values between 800 nm and 880 nm, we monitored the population of the (undressed) bound states (with $n \leq 8$) in time. Even though it is not possible to unambiguously trace the population transfer from one specific state to another, this method still enables us to identify resonances that are relevant for ionization enhancement.

For the co-rotating field, the time-dependent populations are shown in Fig. 7 for 800 nm, 840 nm, and 880 nm light. The dressing of the initial 2p state by the weak laser field occurs mainly via one-photon coupling to the 2s and 3d states, whose populations are seen to adiabatically follow the square of the pulse envelope, leading to the well-known quadratic AC stark shift. It is noteworthy that these states mix strongly, although there is a large frequency detuning to the 2s-2p and 2p-3d transitions at 671 nm and 610 nm, respectively. On the other hand, resonant transitions to the excited 5f and 6f Rydberg states participate very effectively in the ionization enhancement. These states, coupled to the 2p state by two-photon transitions, undergo Rabi-like oscillations [35–37], whose frequency depends on the strength of the coupling, leading to nonnegligible populations at the end of the pulse. The ionization enhancement is strongest at 840 nm due to the coupling between the 2p and 5f states, whose resonance wavelength is 826 nm. In this case, the total ionization probability is more than five times higher than for the other two wavelengths, and a significant fraction of the population (more than 5 %) remains in the excited 5f state after the pulse. At 880 nm, the 4f state is seen to mostly contribute to a quartic AC stark shift via two-photon coupling.

The population distributions for the counter-rotating case are shown in Fig. 8. As expected, prominent Rabi oscillations and a large population transfer (up to 90 %) between the initial 2p and the excited 3s state appear at 800 nm due to the proximity to the resonance. From the 3s state, population can be transferred further up to the continuum using the 6p state as a stepping stone (see Fig. 3), resulting in an ionization probability well above 1 %. At 840 nm, the overall picture remains similar with
a weaker coupling between the 2p and 3s states leading to a slightly reduced ionization probability. Even further off resonance at 880 nm, the amplitudes of the Rabi oscillations are strongly reduced and the 3s population follows the pulse envelope more adiabatically. It is surprising that the ionization rate increases again for this wavelength. However, there are two features of the population distributions that might explain the overall high ionization rate: First, the 3s population is consistently above 10% during the pulse and even approaches 20% when the field intensity reaches its maximum. Second, two-photon excitation of the 4f state is observed as well, which might contribute to the large ionization probability at this wavelength. Overall, the variation of the ionization probability is much smaller for the counter-rotating geometry than for the co-rotating one. Therefore, we attribute the alternating behavior of the $CD$ mainly to the large fluctuations of the ionization probability for the co-rotating field.

This theoretical analysis shows that the ionization rate depends strongly on the coherent population transfer between the initial and intermediate states. Therefore, it is in principle possible to induce sharp variations of the $CD$ through only small variations of the wavelength. Because the populations of the states undergo Rabi oscillations, the $CD$ is also affected by the intensity, duration, and wavelength of the pulse. Since the cross sections are not measured for a single peak intensity but for an intensity range spanning the laser focus, along with other experimental uncertainties, our measured cross sections and $CD$ values represent an average that results in a smoother variation of the $CD$ than in theory. These effects make the identification of intensity-related variations almost impossible, or at least very challenging, from an experimental perspective. Due to the remaining uncertainties and fluctuations in several of the experimental parameters, we did not perform additional calcu-
lutions as they would most likely not shed more light on the interpretation of the experimental data.

It should be noted that there are also significant discrepancies between the measured and calculated CD values at wavelengths of 740 nm, 780 nm, and 840 nm. All these wavelengths are close to two-photon resonances between the 2p and excited np and nf states, which lie around 826-829 nm for n = 5, 780 nm for n = 6, and 744 nm for n = 8. Although we did not perform a detailed investigation of the population distributions for these wavelengths, we expect that two-photon Rabi oscillations with periods close to the pulse duration are also strongly affecting the efficiency of resonance enhancement.

V. SUMMARY AND CONCLUSIONS

In this work, we addressed the question how atomic resonances affect the helicity dependence of the multiphoton ionization of polarized atomic targets in circularly polarized femtosecond laser fields. Specifically, we studied circular dichroism in two- and three-photon ionization of excited and polarized lithium atoms initially in the 2p ({}^2\!P_1) state for wavelengths ranging from 665 nm to 920 nm. Experimentally, we find that the ionization probability is larger for most wavelengths if the electric field vector and the initial electronic current density are co-rotating. However, there is a distinct minimum in the CD value at a wavelength near 800 nm, where the counter-rotating geometry is favored. This feature is qualitatively explained by the 2p-3s resonance, which is only driven for the counter-rotating case, thus resulting in a helicity-selective resonance enhancement.

The comparison of the experimental data to our theoretical model, which is based on the numerical solution of the time-dependent Schrödinger equation, yields good qualitative agreement, although the calculation shows a larger scattering of the CD values and even a second minimum around 880 nm. The theoretical approach allows to extract time-dependent population distributions of the atomic states during and after the femtosecond laser pulse, which helps to shed light on the underlying dynamics and the involved intermediate states. This analysis shows Rabi oscillations between states coupled by one- and two-photon transitions. The populated excited states can result in resonance-enhancement and act as stepping stones for the electrons while they are promoted to the continuum. Because Rabi frequencies and time-dependent excited state populations depend sensitively on the details of the pulse, such as its intensity, duration, and detuning off a resonance, the total ionization probabilities and, therefore, the CD values are expected to be strongly influenced by these parameters as well. In our experiment, the peak intensity of the laser pulse is difficult to control due to the spatial intensity profile of the laser focus in the reaction region. As a result, the experimental CD values represent a weighted average for different intensities.

The present work does not only show the importance of the atomic structure on the ionization probability and the circular dichroism, but it also exposes the significance of details of the pulse parameters on the ionization dynamics.

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