Kirigami Actuators

Marcelo A. Dias,1, 2 Michael P. McCarron,3 Daniel Rayneau-Kirkhope,4 Paul Z. Hanakata,5 David K. Campbell,5 Harold S. Park,3 and Douglas P. Holmes3

1Department of Engineering, Aarhus University, Inge Lehmanns Gade 10, 8000 Aarhus C, Denmark.
2Department of Physics and Astronomy, James Madison University, Harrisonburg, VA 22807, USA.
3Department of Mechanical Engineering, Boston University, Boston, MA, 02215, USA.
4Department of Applied Physics, Aalto University, FI-02150 Espoo, Finland.
5Department of Physics, Boston University, Boston, MA 02215, USA.

(Dated: October 10, 2017)

Thin elastic sheets bend easily and, if they are patterned with cuts, can deform in sophisticated ways. Here we show that carefully tuning the location and arrangement of cuts within thin sheets enables the design of mechanical actuators that scale down to atomically–thin 2D materials. We first show that by understanding the mechanics of a single, non–propagating crack in a sheet we can generate four fundamental forms of linear actuation: roll, pitch, yaw, and lift. Our analytical model shows that these deformations are only weakly dependent on thickness, which we confirm with experiments at centimeter scale objects and molecular dynamics simulations of graphene and MoS2 nanoscale sheets. We show how the interactions between non–propagating cracks can enable either lift or rotation, and we use a combination of experiments, theory, continuum computational analysis, and molecular dynamics simulations to provide mechanistic insights into the geometric and topological design of kirigami actuators.

Deformations that bend a material without stretching involve a very low amount of stored elastic energy, and therefore present an opportunity to enable morphing at minimal energetic cost. The potential to exploit these energetically favorable and soft modes has recently emerged with kirigami-based thin sheets [11,12], in which the introduction of cuts has been utilized to give unique structural properties and non-linear behavior, such as auxeticity [13–15], significantly enhanced stretchability [16,17], flexible electronic devices [18,19], and topologically guided morphings [20,21]. In this work, we present a variety of kirigami actuators whose dynamical pattern formation is controllable. We develop a novel form of non-linear control-response relationships in kirigami geometries through the conversion of linear displacement imposed on the boundary of the thin sheet into a range of predictable motions.

The four fundamental modes depicted in figure 1, namely roll (rotation about x–axis), pitch (rotation about y–axis), yaw (rotation about z–axis), and lift (z–axis out–of–plane displacement), arise from linear actuation, and they may in principle be combined to generate any motion in 3D space. To demonstrate this designing goal, we create three orthogonal rotations and a vertical out–of–plane displacement and show the mechanism for understanding how these emerge from the coupled behavior of individual cuts. We provide a theory that captures the main large scale features in the mechanics of these structures, and demonstrate that similar actuators can be realized in suspended 2D materials, such as graphene and MoS2 [17,18]. Moreover, a full characterization of the out–of–plane displacement that occurs as a result of a single cut in a thin sheet allows us to derive a scaling law that shows a robust link between simulation and experiment on length–scales ranging over six orders of magnitude. Because kirigami actuators are scale–invariant, our findings can be applied to tailor the microstructure and functionality of mechanical metamaterials across the technological spectrum of length scales ranging from the nanoscale (NEMS) [17,20], the microscale (MEMS) [21–24], and the macroscale [25,26].

The complex behavior of kirigami actuators arises from functionalizing cracks in thin plates. In other words, when a material is thin enough, cracks under tension may cause the system to buckle before failure through crack propagation [29,30]. Therefore, a deeper understanding of the mechanics of a single non–propagating crack on thin sheets is needed. Let us consider a cut of length b centered with respect to the sheet’s length L and width w, and parallel to the clamped edges of the sheet (figure 2). The sheet thickness h is small, such that $h \ll L \sim w$. Applying a uniaxial extension $\Delta$ perpendicular to the crack causes the sheet to buckle out–of–plane at a critical force $F_c$. The typical deflection size is given by a maximum amplitude $\delta_0$ centered between the crack tips, and this shape decays back to nearly flat before reaching the clamped boundaries (figure 2). This characteristic shape occurs on each side of the crack, such that the shape may be symmetric or antisymmetric about the plane aligned with the crack, normal to the initially flat surface—these two modes, respectively, correspond to stress intensity factors of bending and transverse shear [29,31]. We shall here focus our analysis on the symmetric kind, as the typical size of both out–of–plane deformations must be of the same order of magnitude. The critical force needed to trigger this instability is given by $F_c$, which depends on the ratio of the crack to sheet width, $b/w$ (figure 2). Since the instabil-
FIG. 1. Examples of linear actuators from kirigami cut patterns. Extension, or applied displacement $\Delta$, along the $x$-direction causes a. rotation about $y$–axis or pitch, b. rotation about $z$–axis or yaw, c. rotation about $x$–axis or roll, and d. out–of–plane deflection in the $z$-direction.

ity results from an in–plane compressive zone (figure 2a) around the internal boundary along the crack [30, 32], this problem will be approximated by a beam of length $b$. Therefore, $F_c$ is shown to collapse on a single curve (figure 2c) when the experimental data and simulation results are normalized by the characteristic buckling force $Eh\Delta_c$, where $E$ is the Young’s modulus of the material. This will become evident in equation (5), where we derive $\Delta_c \equiv h^2/b$ as the critical amount of in–plane compression at the buckling threshold.

To describe the post–buckled shape, we consider two regimes: the in–plane stretching dominated response to an applied extension $\Delta$ normal to the single cut, and the out–of–plane state, where the buckling threshold is reached in the stress relief zone and the system becomes bending dominated. This loading condition induces a crack opening mode described by the mode I stress intensity factor, $K_I$, which for a large plate in a state of uniform uniaxial stress is $K_I = T\sqrt{\pi b}2$, where $T$ is the tensile stress acting on the edge of the sheet [33]. From fracture mechanics [33], it is established that the stress scales with the radius of curvature $r$ of the cut: $\sigma = K_I/\sqrt{2\pi r}$. To estimate the tension in the sheet, we note that stresses concentrate near the crack and, in view of St. Venant’s Principle [34], it approaches an average value at a distance of about width $w$ away from the crack. This approximation is also validated from the fact that beyond a sheet length to width ratio of about $L/w \approx 1$, the maximum deflection of the crack reaches a constant value indicating that, beyond a certain point, the sheet length does not contribute to the crack deformation. Therefore, we expect the tension in the sheet to scale as $T \sim E\Delta/w$. In our experiments we take $r \sim h$ for the crack radius. Therefore, the stress in the sheet becomes $\sigma \sim E(\Delta/w)(h/h)^{1/2}$. The elastic strain energy due to stretching scales as $U_s \sim h (\sigma^2/E) A_s$, where

FIG. 2. a. Single cut’s in–plane state of stress calculated from Finite Element method (FEM). Simulation parameters are set based on the experiments: $h = 0.127\text{mm}$, $b = 80\text{mm}$, $w = 100\text{mm}$, $L = 182\text{mm}$, Young’s Modulus $E = 3.5\text{GPa}$, Poisson’s ratio $\nu = 0.38$, and $\Delta \sim h$. The color map shows the normalized sum of the principal stresses. b. First mode of deformation, where color map represents the normalized deflection, $\delta/\delta_0$. c. Critical force $F_c$ required for buckling near the crack as a function of $b/w$. FEM simulation (solid lines) and experimental (disks with error bars) are shown. d. Plot of $\delta^2/\delta_0^2$ as a function of $\Delta/w$ for experiments with mylar films (circles), FEM simulations (solid lines), and MD simulations of graphene (squares) and MoS2 (triangles). The scaling from equation (4) is represented by the dashed line. Mylar and FEM parameters are set to $h = 0.127\text{mm}$, $L = 182\text{mm}$, $E = 3.5\text{GPa}$, and $\nu = 0.38$. MD simulations were done for a fixed $L = 346\text{Å}$, we plot date for width $w = 114\text{Å}$ and cuts lengths ranging from $b = 38\text{Å}$ to 76Å, and for $w = 142\text{Å}$ with cuts ranging from $b = 81\text{Å}$ to 119Å. e. Shows a suspended graphene sheet ($b = 76\text{Å}$, $w = 114\text{Å}$, $L = 346\text{Å}$, $\Delta = 40\text{Å}$), where the color map shows the von Mises stress scaled by its maximum value.
the lift of the center of the sheet to significantly drop.

c.
generating lift.

b.
ure 2

a 1D buckling of the free boundary along the crack (fig-

The calculation is simplified by treating the problem as
to reduce the total energy through out–of–plane bending.

bution by allowing the stresses in the compressive zone
son’s contraction and sets up the base state for the in–

s

given by

\[ U_s \sim E \Delta^2_w bL. \]  

(1)

If we consider the sheet to be dominated by stretching,
\textit{i.e.} by initially neglecting bending energy, the total po-
tential energy is given as \( V = U_s - W \), where \( W \) is the
work done by the extension \( \Delta \). Taking the work as the
force \( (E \gamma^{(0)}) A_s \) times the extension \( \Delta \), where \( \gamma^{(0)} \) is la-
teral strain of the sheet, and minimizing the total poten-
tial energy, \( (\partial / \partial \Delta) \left[ E (\Delta^2/w) bL - E \gamma^{(0)} Lw \Delta \right] = 0 \),
gives a relation for the lateral contraction,

\[ \Delta_\perp \equiv \gamma^{(0)} w \sim b \Delta/w. \]  

(2)

Note that equation (2) is effectively a scaling of Pois-
son’s contraction and sets up the base state for the in-
plane solution. We now calculate the next order con-
tribution by allowing the stresses in the compressive zone
to reduce the total energy through out–of–plane bending.
The calculation is simplified by treating the problem as
a 1D buckling of the free boundary along the crack (fig-
ure 2b), where both stretching and bending energies are
required to provide the right balance. This next order con-
ntribution is obtained as a minimizer of a dimension-
ally reduced model, along the arc-length \( s \) of the cut,
given by

\[ U = \frac{bhE}{2} \int ds \left[ \gamma^2 + h^2 \delta''^2 \right], \]  

(3)

where the new measure of strain is geometrically non-
linear, \( \gamma \approx \gamma^{(0)} + \delta''^2/2 \), and \( \delta \) is the deflection.
This yields a classic result for the maximum amplitude:

\[ \delta_0 \sim \sqrt{\delta} \sqrt{\Delta_\perp - \Delta_c}, \]  

(4)

where \( \Delta_c \) is related to the ratio between bending rigid-
ity, \( B = h^3 E \), and stretching rigidity, \( Y = h E \), as follows:

\[ \Delta_c/b \sim (b^2 Y) = (h/b)^2. \]  

Inserting the in–plane com-
pression result of equation (2) into (4) gives a scaling for
the maximum crack deflection,

\[ \left( \frac{\delta_0}{b} \right)^2 \sim \frac{\Delta}{w} - O \left( \frac{h}{b} \right)^2. \]  

(5)

Equation 5 shows a higher order dependency on the
sheet thickness to crack length ratio, implying the in-
variance of these deformations from the macro to the
nanoscale. To confirm this relationship, experiments were
performed with single cuts in mylar films (Biaxially-
oriented polyethylene terephthalate—BoPET) to mea-
Sure the maximum deflection as a function of extension
for a given crack size and sheet width (see methods sec-
tion). Finite Element Method (FEM) simulations with
the same material parameters were also performed (see
methods section). Additionally, we carried out Molecu-
lar Dynamics (MD) simulations of suspended graphene
monolayers (see methods section). Figure 2a shows the
dimensionless deflection data for the experiments and
simulations, along with the scaling prediction from equa-
tion 5, confirming a very strong agreement across six or-
ders of magnitude.

In order to generate simple actuators that can become
the building blocks for more complex structures, such as
mechanical metamaterials, we must quantify how mul-
tiple cracks will interact to generate motion of points
on the sheet. Since the behavior of a single crack is
well described by equation 5, the simplest extension is
two parallel cracks of length \( b \) separated by distance \( \ell_s \).
When \( \ell_s/L \) is small, these cracks interact to gen-
erate vertical lift of the sheet between them (figure 3i–i & ii).
However, the deflection of the center point of the
sheet drops off quickly as the spacing between the cracks
is increased, making it difficult to lift a large amount of
surface area (figure 3h). Keeping \( \ell_s/L \) small while in-
creasing the area of the sheet that is lifted can be accom-
plished by extending a portion of each crack towards the
clamped boundaries (figure 3l–iii). This relies on the
same buckling mechanism that governs the single crack
behavior, producing nearly the same amount of lift as the
two parallel cracks (figure 3a). These additional cuts also
introduce wrinkles on the sheet, which can be avoided by
introducing cuts that provide room for in–plane compres-
sion (figure 3i–iv). With this arrangement of cuts, we
demonstrate how these parallel cracks can become build-
ing blocks for generating lift of a large, localized area.

We note that the four crack tips of the two parallel
cracks in figure 3h–i form a rectangular unit cell (convex
polygon) and generate lift in the sheet. This rudimentary
shape is identified quantitatively by following the lines
of tension that connect two neighboring cracks, and the
convexity of the unit cell signifies how much stretching
within the sheet can be transferred into a crack opening
displacement. Convex shapes constrain the sheet to in-
duce vertical lift, while concave shapes have the freedom

A_s = Lw is the area of the sheet, which reduces to

\[ A_s = Lw \]
FIG. 4.  

a. Schematics illustrating how the polygon formed by crack tips will generate rotation. b. As the polygon formed by the edge crack tip and the internal crack tips changes from convex to concave, we see the emergence of rotation about the $y$–axis. c. The coupling of multiple concave polygons formed by the crack tips can enable rotation about the $x$ or $z$ axis as well.

to rotate. To illustrate this idea, we focus on the pitch mode. We performed a post–buckling analysis through FEM simulations for the geometry in figure 4a, while varying crack length $L_c$, thus allowing us to scan unit cell shapes from convex to concave. Denoting $L_\parallel$ as the cut length parallel to the clamped boundary, we refer to the ratio $(2L_c + L_\parallel)/w$ as a measure of convexity. The target shape strongly depends on this parameter’s transition: lift of the outer portion of the sheet occurs when the unit cell is convex, i.e. $(2L_c + L_\parallel)/w < 1$, while rotation about the $y$–axis occurs when it is concave, i.e. $(2L_c + L_\parallel)/w \gtrsim 1$ (figure 4b). Generating rotation about the $z$ and $x$ axes follows the same principle—concave unit cells enable rotation (figure 4c). In these more complex configurations, there is coupling between two unit cells within the sheet. While an intricate model of the coupling between multiple unit cells is beyond the scope of this work, it is clear from the schematics and post–buckled shapes that the concave unit cells locally enable rotation about the $z$ and $x$ axes.

Figure 4 indicates that the convexity of the unit cell formed by the locally interacting crack tips can generate either lift or rotation. We provide further insight through quantifying the magnitude of these kirigami–based motions by measuring the lift or rotation as a function of relative strain $\Delta/L$ (figure 5). Here we show that a portion of the sheet can achieve a vertical displacement nearly 50 times the sheet thickness. Since there is no plastic deformation and the cracks do not propagate, these deformations are reversible. The stiffness of the sheets designed to provide rotation varies widely. Rotations about the $y$ (pitch) and $x$ (roll) axes reach about 60 degrees after a moderate amount of extension, while the in–plane rotation about $z$–axis requires a significant amount of extension to reach 30 degrees of rotation. Figure 5a shows good agreement between the experimental measurements for the macroscale designs of lift ($\delta_0$) and rotation (triangles for $\theta_x$, disks for $\theta_y$, and squares for $\theta_z$) and the FEM simulations (dashed line for $\delta_0$, orange for $\theta_x$, red for $\theta_y$, and blue for $\theta_z$).

The results from figure 2d suggest that these actuator designs should scale down to 2D materials. From a MoS$_2$ monolayer, we tested the simplest nanoactuator requiring only one unit cell for rotation about the

FIG. 5.  

a. A plot of the lift of the center $\delta_0$ (black) and the three rotations as functions of $\Delta/L$, $\Delta$ being the applied displacement in the $x$–direction. The experimental data corresponds to black diamond for lift, orange triangles for the roll (rotation about $x$–axis), red disks for the pitch (rotation about $y$–axis), and blue squares for the yaw (rotation about $z$–axis). FEM for the respective modes of deformation, using the same parameters of the experiments, are shown in dashed and solid curves. The red x’s show the results of the molecular dynamics simulations.  

b. Images of the experiments for the cut patterns and the sequence of deformation as $\Delta/L$ is increased as well as two snapshots of the molecular dynamics simulation. In the case of the MoS$_2$, the geometric parameters are: length $L = 460\text{Å}$ and width $w = 152\text{Å}$ of the sheet; crack length $L_c = 47.5\text{Å}$; and a 240Å length and a 82Å width ($L_\parallel$) of the inner rotating ribbon.
quently lift in the $z$-axis, i.e. the pitch mode shown at the bottom in figure [3]. We obtained a rigid rotation due to its higher bending modulus than that of graphene [35]. We applied an extension perpendicular to the crack and measured the rotation of the inner ribbon about the $y$-axis (figure [3p, red x’s). At small $\Delta/L$, there is good agreement between the macroscale results and the nanoscale simulations, and eventually the three actuators achieve nearly the same maximum value of $\theta_y$. While the behavior is qualitatively similar across several orders of magnitude in sheet thickness, it is clear that the agreement for the 2D kirigami is qualitative rather than quantitative. Specifically, the fact that the rotation that is observed in the 2D kirigami is smaller for the same strains than the bulk system suggests that the 2D system may undergo more stretching than the bulk system, a point also made recently by Grosso and Mele [36]. Therefore, additional analysis of the 2D material kirigami actuators is necessary to quantitatively replicate the macroscale actuator designs.

Finally, we return to the actuators in figure 1. Through replicating the mechanism in figure 3a, we see rotation about the $y$-axis of all cells (Figure 1b). This indicates that building blocks can go beyond mechanism design towards the development of mechanical metamaterials. Furthermore, the interactions between multiple cuts can enable portions of a thin sheet to rotate one complete revolution about the $x$-axis the extension axis (figure 1c), while coupling unit cells that cause rotation and lift generates sheets that first rotate about the $y$-axis and subsequently lift in the $z$ direction (figure 1d). What remains is to better understand how building blocks can be combined to generate targeted behaviors—an inverse problem that can begin by considering the simple geometric model we present here.

We have addressed two fundamental problems that are pivotal to connecting kirigami actuators to practical designs for engineering applications: scale-invariant behavior and a robust geometric mechanism for actuator design. While the kirigami mechanics has been unified over six orders of magnitude in sheet thickness, the shape of a unit cell formed by locally interacting crack tips provides a geometric mechanism to induce either lift or rotation. What we present has the potential to offer rational designing tools for dynamical assembling of complex geometries [10–28], and we hope that this spontaneous generation of shapes emerging from quasi-static actuation comes to complement inverse design algorithms that have been proposed for lattice-based kirigami [14, 15]. As it has been previously mentioned, the cracks do not propagate in the experiments performed here, thus the process remains entirely reversible. In order to maintain this reversibility in systems utilizing materials with lower yield stress, cracks can be made with a larger crack tip radius $r$, thus lowering the stress intensity factor, $K_I$. The scaling found here is robust under such a modification since a few multiples of $r$ only yield a pre-factor in front of equation (9), thus preserving the same power-law. It is also noted that the propagation of interacting cracks can be manipulated by their initial geometry [37, 38], such interactions could be utilized to increase the functionality of the kirigami structures and/or give a predictable response to strain beyond that which causes crack propagation. There may also be significant scientific benefits to demonstrating kirigami actuation in 2D materials. From a basic science perspective, kirigami provides an ideal platform to study the localization of electronic states, or the coupling of 2D quantum dots [39]. Alternatively, these structures offer significant opportunities for flexible, lightweight band-gap engineered optoelectronic materials whose performance can be reversibly changed and manipulated over a wide range of the optical spectrum by locally varying the strain [40–47].

**METHODS SECTION**

**Fabrication:** Mylar (BoPET) films were purchased from McMaster–Carr (Mylar, 8567K96), and had a thickness of $h = 0.127$ mm. To relieve any residual stress in the films, apparent from their natural curvature, we annealed the films in the oven at $85^\circ C$ under the weight of thick metal sheets for 2 hours, resulting in flat sheets. Vector patterns were drawn in Adobe Illustrator CS6, and cut with an Epilog Mini 24, 75W laser cutter in vector mode, at 80% speed and 10% power. Sheet widths of $w = 40$mm, 60mm, 80mm, and 100mm were used, and sheet lengths of $L = 20$mm to 200mm in linear increments of 20mm were used. For the single cut experiments, cut lengths ranging from $b = 20$mm to 70mm were used. The cut mylar films were adhered to 3mm thick acrylic sheets (McMaster–Carr, acrylic, 8560K191) with cyanoacrylate glue (McMaster–Carr, Loctite 403, 74765A53), which served as the clamped boundary conditions for the films.

**Mechanical Measurements:** Uniaxial tension tests were performed by clamping the mylar sheets to the Instron 5943 mechanical testing system, using a 500N load cell. Displacement–controlled tests were performed at a rate of 0.15mm/min to a maximum extension of 1.5mm. Since the mylar did not experience inelastic strains, actuation was reversible, and 3 tests were run for each sample. Actuator deformation was captured from the side with a microscopic lens (Navitar Zoom 6000) attached to a Nikon D610 camera, and from the front using a Nikon D610 camera with a Micro-NIKKOR 105mm f/2.8 Lens, a Nikon 55mm f/2.8 Lens, and a high contrast Rosco Color Filter (B&H Photo Video, ROCEK1212). The critical buckling force was determined from identifying both the slope change in the force vs. displacement curve, and the out–of–plane deflection from the microscopic imaging of the crack profile.

**Finite Element Method (FEM):** FEM simulations were undertaken using COMSOL Multiphysics 5.2 [48] along with the Structural Mechanics Module. Shell Mechanics and Plates were the environments within COMSOL.
in which all of our studies were performed. A geometry matching those used in the experiment was created in COMSOL’s Design Module. Mesh refinement studies were undertaken to ensure convergence of the results. For the single cut geometry in figure 2, the sheet was modeled as an isotropic elastic thin sheet with thickness of \( h = 0.127 \text{mm} \), Young’s Modulus \( E = 3.5 \text{GPa} \), and Poisson’s ratio \( \nu = 0.38 \). The results shown in figure 2c were attained through linear buckling studies with varying thickness in the range \( h \in [0.1 \text{mm}, 0.14 \text{mm}] \) and the values \( b/w \in [0.3, 0.8] \). The in-plane results shown in figure 2a and post-buckling results in figures 2d, 3, and 4 were calculated from a stationary study with displacement (\( \Delta \)) controlled analysis. In order to induce out-of-plane symmetry breaking, we added random small imperfections (ten orders of magnitude smaller than the sheet thickness) to the initial surface. The parameters in figure 2a were attained through linear buckling studies with varying thickness in the range \( h \in [0.1 \text{mm}, 0.14 \text{mm}] \) and the values \( b/w \in [0.3, 0.8] \). The in-plane results shown in figure 2d varied and lay in the ranges \( h \in [0.15 \text{mm}, 0.21 \text{mm}] \) and \( b/w \in [0.1, 0.9] \). For the results shown in figure 5, linear buckling studies were undertaken with the boundary at \( x = 0 \) fixed in space while the boundary at \( x = L \) had an imposed displacement of \( \Delta \) in the \( x \) direction. Both of these boundaries were not permitted to rotate. All other boundaries were free. Small imperfections in the form of the first eigenmodes were then added to the initially flat geometry through use of MeshPerturb 1.0 \[49\]. These imperfect geometries were then used for the stationary studies with the same boundary conditions and the same mesh density as was used in the linear studies.

Molecular Simulations: We used Sandia-developed open source LAMMPS Molecular Dynamics Simulator to simulate graphene sheets \[50\]. To describe the carbon-carbon interactions, we used AIREBO potential \[51\] as has been used previously in atomistic study of graphene kirigami \[17\]. The cutoffs for the Lennard-Jones and the REBO term in AIREBO potential are chosen to be 2 Å and 6.8 Å, respectively. For MoS\(_2\) actuators we used the Stillinger-Weber potential developed by Jiang \[52\], which we have previously employed to study MoS\(_2\) kirigami \[53\]. Graphene with a single crack and the MoS\(_2\) actuator were first relaxed for 50–200 ps at 4.2K within the NVT (fixed number of atoms \( N \), volume \( V \), and temperature \( T \)) ensemble. Non-periodic boundary conditions were applied in all three directions. After the relaxation, the strains were applied by displacing both ends at a uniform rate.

**AUTHOR CONTRIBUTIONS**

M.A.D. and D.P.H. conceived the study and proposed the research; M.A.D. and D.R.K. performed the mathematical modeling and FEM in consultation with D.P.H.; M.P.M. and D.P.H. performed the experiments in consultation with M.A.D.; P.Z.H., D.K.C., and H.S.P. performed the Molecular Simulations studies; M.A.D. and D.P.H. wrote the main article; and all authors jointly edited the entire article.

**ACKNOWLEDGEMENTS**

M.A.D. is grateful to M. Adda-Bedia, J. Bico, B. Roman, and K. Seffen for many insightful discussions. M.A.D. would also like to thank ENS-Lyon and ESPCI-Paris for hosting the author during part of the development of this manuscript and funding from the 4-VA program for collaborative research at JMU. D.P.H. is grateful to the National Science Foundation (CMII CAREER–1454153) for financial support. M.A.D., D.R.K., and D.P.H. would like to thank I. Metta for the useful discussions at the start of this project. D.K.C. acknowledges the Aspen Center for Physics, which is supported by National Science Foundation grant PHY-1607611, where part of this work was completed. D.R.K. acknowledges funding from Academy of Finland.

**CONFLICT OF INTEREST**

The authors declare no conflict of interest.

[1] P. M. Reis, Journal of Applied Mechanics 82, 111001 (2015).
[2] K. A. Seffen, Physical Review E 94, 033003 (2016).
[3] A. Rafsanjani and K. Bertoldi, Physical Review Letters 118, 084301 (2017).
[4] J. Bico, E. Lepoivre, H. Bense, E. Reyssat, and B. Roman, Bulletin of the American Physical Society 62 (2017).
[5] K. Virk, A. Monti, T. Trehard, M. Marsh, K. Hazra, K. Boba, C. D. L. Remillat, F. Scarpa, and I. R. Farrow, Smart Materials and Structures 22, 084014 (2013).
[6] F. Scarpa, M. Ouisse, M. Collet, and K. Saito, Journal of Vibration and Acoustics 135, 041001 (2013).
[7] Y. Tang and J. Yin, Extreme Mechanics Letters 12, 77 (2017).
[8] T. C. Shyu, P. F. Damasceno, P. M. Dodd, A. Lamoureux, L. Xu, M. Shlian, M. Shtein, S. C. Glotzer, and N. A. Kotov, Nature materials 14, 785 (2015).
[9] N. Vachicouras, C. M. Tringides, P. B. Campiche, and S. P. Lacour, Extreme Mechanics Letters 15, 63 (2017).
[10] Y. Zhang, Z. Yan, K. Nan, D. Xiao, Y. Liu, H. Luan, H. Fu, X. Wang, Q. Yang, J. Wang, et al., Proceedings of the National Academy of Sciences 112, 11757 (2015).
[11] J.-F. Sadoc, N. Rivier, and J. Charvolin, Acta Crystallographica Section A: Foundations of Crystallography 68, 470 (2012).
[12] J. Charvolin and J.-F. Sadoc, Biophysical Reviews and Letters 6, 13 (2011).
[13] J.-F. Sadoc, J. Charvolin, and N. Rivier, Journal of Physics A: Mathematical and Theoretical 46, 295202 (2013).
[14] T. Castle, Y. Cho, X. Gong, E. Jung, D. M. Sussman, S. Yang, and R. D. Kamien, Physical Review Letters 113, 1 (2014).
[15] D. M. Sussman, Y. Cho, T. Castle, X. Gong, E. Jung, S. Yang, and R. D. Kamien, Proceedings of the National Academy of Sciences p. 201506048 (2015).
[16] B.-g. Chen, B. Liu, A. A. Evans, J. Paulose, I. Cohen, V. Vitelli, and C. D. Santangelo, Physical review letters 116, 135501 (2016).
[17] Z. Qi, D. K. Campbell, and H. S. Park, Physical Review B 90, 245437 (2014).
[18] B. G.-g. Chen, B. Liu, A. A. Evans, J. Paulose, I. Cohen, V. Vitelli, and C. D. Santangelo, Physical review letters 116, 135501 (2016).
[19] Z. Qi, D. K. Campbell, and H. S. Park, Physical Review B 90, 245437 (2014).
[20] M. K. Blees, A. W. Barnard, P. A. Rose, S. P. Roberts, K. L. McGill, P. Y. Huang, A. R. Ruyack, J. W. Kevek, B. Kobrin, D. A. Muller, et al., Nature 524, 204 (2015).
[21] K. Cai, J. Luo, Y. Ling, J. Wan, and Q.-H. Qin, Scientific Reports 6 (2016).
[22] T. Han, F. Scarpa, and N. L. Allan, Thin Solid Films (2017).
[23] Z. Song, X. Wang, C. Lv, Y. An, M. Liang, T. Ma, D. He, Y.-J. Zheng, S.-Q. Huang, H. Yu, et al., Scientific reports 5, 10988 (2015).
[24] M. K. Blees, A. W. Barnard, P. A. Rose, S. P. Roberts, K. L. McGill, P. Y. Huang, A. R. Ruyack, J. W. Kevek, B. Kobrin, D. A. Muller, et al., Nature 524, 204 (2015).
[25] Z. Qi, D. K. Campbell, and H. S. Park, Physical Review B 90, 245437 (2014).
[26] M. K. Blees, A. W. Barnard, P. A. Rose, S. P. Roberts, K. L. McGill, P. Y. Huang, A. R. Ruyack, J. W. Kevek, B. Kobrin, D. A. Muller, et al., Nature 524, 204 (2015).
[27] K. Cai, J. Luo, Y. Ling, J. Wan, and Q.-H. Qin, Scientific Reports 6 (2016).
[28] T. Han, F. Scarpa, and N. L. Allan, Thin Solid Films (2017).
[29] Z. Song, X. Wang, C. Lv, Y. An, M. Liang, T. Ma, D. He, Y.-J. Zheng, S.-Q. Huang, H. Yu, et al., Scientific reports 5, 10988 (2015).
[30] M. K. Blees, A. W. Barnard, P. A. Rose, S. P. Roberts, K. L. McGill, P. Y. Huang, A. R. Ruyack, J. W. Kevek, B. Kobrin, D. A. Muller, et al., Nature 524, 204 (2015).
[31] Z. Qi, D. K. Campbell, and H. S. Park, Physical Review B 90, 245437 (2014).
[32] M. K. Blees, A. W. Barnard, P. A. Rose, S. P. Roberts, K. L. McGill, P. Y. Huang, A. R. Ruyack, J. W. Kevek, B. Kobrin, D. A. Muller, et al., Nature 524, 204 (2015).
[33] Z. Qi, D. K. Campbell, and H. S. Park, Physical Review B 90, 245437 (2014).
[34] M. K. Blees, A. W. Barnard, P. A. Rose, S. P. Roberts, K. L. McGill, P. Y. Huang, A. R. Ruyack, J. W. Kevek, B. Kobrin, D. A. Muller, et al., Nature 524, 204 (2015).
[35] Z. Qi, D. K. Campbell, and H. S. Park, Physical Review B 90, 245437 (2014).
[36] M.-Y. Tsai, A. Tarasov, Z. R. Hesabi, H. Taghinejad, P. M. Campbell, C. A. Joiner, A. Adibi, and E. M. Vogel, ACS applied materials & interfaces 7, 12850 (2015).
[37] K. He, C. Poole, K. F. Mak, and J. Shan, Nano letters 13, 2931 (2013).
[38] D. Lloyd, X. Liu, J. W. Christopher, L. Cantley, A. Wedehra, B. L. Kim, B. B. Goldberg, A. K. Swan, and J. S. Bunch, Nano letters 16, 5836 (2016).
[39] J. Feng, X. Qian, C.-W. Huang, and J. Li, Nature Photonics 6, 866 (2012).
[40] H. J. Conley, B. Wang, J. I. Ziegler, R. F. Haglund Jr, S. T. Pantelides, and K. I. Bolotin, Nano letters 13, 3626 (2013).
[41] J.-W. Jiang, Z. Qi, H. S. Park, V. M. Pereira, and D. K. Campbell, Phys. Rev. B 93, 235408 (2016), URL https://link.aps.org/doi/10.1103/PhysRevB.93.235408.