Linear Free Energy Relationships for Enzymatic Reactions: Fresh Insight from a Venerable Probe

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CONSPECTUS: Linear free energy relationships (LFERs) for substituent effects on reactions that proceed through similar transition states provide insight into transition state structures. A classical approach to the analysis of LFERs showed that differences in the slopes of Bronsted correlations for addition of substituted alkyl alcohols to ring-substituted 1-phenylethyl carbocations and to the β-galactopyranosyl carbocation intermediate of reactions catalyzed by β-galactosidase provide evidence that the enzyme catalyst modifies the curvature of the energy surface at the saddle point for the transition state for nucleophile addition. We have worked to generalize the use of LFERs in the determination of enzyme mechanisms. The defining property of enzyme catalysts is their specificity for binding the transition state with a much higher affinity than the substrate. Triosephosphate isomerase (TIM), orotidine 5′-monophosphate decarboxylase (OMPDC), and glycerol 3-phosphate dehydrogenase (GPDH) show effective catalysis of reactions of phosphorylated substrates and strong phosphate dianion activation of reactions of phosphodianion truncated substrates, with rate constants \( k_{cat}/K_m \) and \( k_{cat}/K_{HPi} \), respectively. Good linear logarithmic correlations, with a slope of 1.1, between these kinetic parameters determined for reactions catalyzed by five or more variant forms of each catalyst are observed, where the protein substitutions are mainly at side chains which function to stabilize the cage complex between the enzyme and substrate. This shows that the enzyme-catalyzed reactions of a whole substrate and substrate pieces proceed through transition states of similar structures. It provides support for the proposal that the diatomic energy of whole phosphodianion substrates and of phosphate dianion is used to drive the conversion of these protein catalysts from flexible and entropically rich ground states to stiff and catalytically active Michaelis complexes that show the same activity toward catalysis of the reactions of whole and phosphodianion truncated substrates. There is a good linear correlation, with a slope of 0.73, between values of the dissociation constants \( K_r \) for release of the transition state analog phosphoglycolate (PGA) trianion and log \( k_{cat}/K_m \) for isomerization of GAP dehydrogenase and variants of TIM. This correlation shows that the substituted amino acid side chains act to stabilize the complex between TIM and the PGA trianion and that ca. 70% of this stabilization is observed at the transition state for substrate deprotonation. The correlation provides evidence that these side chains function to enhance the basicity of the E165 side chain of TIM, which deprotonates the bound carbon acid substrate. There is a good linear correlation, with a slope of 0.74, between the values of \( \Delta G^2 \) and \( \Delta G^0 \) determined by electron valence bond (EVB) calculations to model deprotonation of dihydroxyacetone phosphate (DHAP) in water and when bound to wild-type and variant forms of TIM to form the enediolate reaction intermediate. This correlation provides evidence that the stabilizing interactions of the transition state for TIM-catalyzed deprotonation of DHAP are optimized by placement of amino acid side chains in positions that provide for the maximum stabilization of the charged reaction intermediate, relative to the neutral substrate.

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between dissociation constants \( \log K_i \) for release of the transition state analog phosphoglycolate trianion from wild-type and variants of TIM and \( \log k_{cat}/K_m \) for the respective enzyme-catalyzed isomerization reactions of GAP.

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1. INTRODUCTION

The Hammett equation was used to establish linear free energy relationships (LFERs) between the effect of aromatic ring substituents \( X \) on \( \Delta G^\circ \) for the reference ionization of substituted benzoic acids in water and on \( \Delta G^\circ \) or \( \Delta G^\ddagger \) for reactions at second aromatic frameworks (Figure 1). This equation spurred the characterization of other LFERs, including those correlated by equations developed by Taft, Brunsted, and Grunwald and Winstein. These LFERs are a cornerstone of physical organic chemistry.

Figure 2A shows a pair of reactions for which a LFER is observed. The correlation between \( \Delta G^\circ \) for ionization of substituted phenylacetic and benzoic acids in water, with a slope of 0.5, is consistent with a 2-fold falloff in electrostatic interactions between the ring substituent X and the reacting –COOH that arises from insertion of the methylene group. The slopes determined for Brunsted correlations of \( \log k \) against the \( pK_a \) of varied reactants, such as Brunsted acid (slope of \( \alpha \)) or base (slope of \( \beta \)) catalysts, or reacting alkyl alcohol nucleophiles (slope of \( \beta_{nuc} \)) or alkoxy leaving groups (slope of \( \beta_{nuc} \)) generally lie between 0 and 1.0. These slopes provide a metric for the change in the effective charge “seen” by the varied substituent on proceeding to the reaction transition state, relative to the 1.0 unit change in the charge for the reference ionization reaction.

Brunsted coefficients provide insight into changes in bonding interactions during steps that are not easily probed by kinetic experiments. For example, the value of \( \beta_{nuc} \)obs = –0.1 determined for phosphoryl transfer from phosphorylated pyridine to 3-substituted quinuclidines in water requires a surprising decrease in the effective positive charge at the quinuclidine nitrogen at the transition state for the phosphoryl transfer reaction, so that the reacting amine nitrogen must carry a partial positive charge at the ground state in water. These results were rationalized by Scheme 1, where \( \beta_{nuc} \)eff = –0.2 for removal of a hydrogen-bonded water from the tertiary amine nucleophile to form the desolvated encounter complex with the phosphorylated pyridine has a larger absolute value than \( \beta_{nuc} \)rel = 0.1 for conversion of this encounter complex to the reaction transition state. There is a similar decrease in amine reactivity, with increasing amine basicity, for nucleophilic addition of amines to the 1-(methylthiophenyl)-2,2,2-trifluoroethyl carbocation.

2. BEGINNINGS

J.P.R. first encountered the Brunsted equation in studies on addition of alkyl alcohols to ring-substituted 1-phenylethyl carbocations. The values of \( \beta_{nuc} \) for these reactions (Figure 2B, no general base catalysis), determined as the slopes of correlations of \( \log k_{ac} \) against alcohol \( pK_a \) were found to increase from \( \beta_{nuc} \)eff = 0.1 to \( \beta_{nuc} \)rel = 0.5 as the carbocation is stabilized by a change in the aromatic ring substituent from \( Z = 4-OCH_3 \) to 4-NMe2 (Figure 2B). This increase in the effective transition state positive charge at the oxygen nucleophile, with the decreasing thermodynamic driving force for carboxylation addition, arises from a Hammond-type shift from a reactant to product-like transition state, where there is an increase in bonding between the oxygen nucleophile and carbon electrophile.

These addition reactions of alcohols are catalyzed by alkane carboxylate anions, with third-order rate constants \( k_{ac} \) (Figure 2B). The slopes of Brunsted-type correlations of \( \log k_{ac} \) against the \( pK_a \) of the conjugate acid of the catalyst increase from \( \beta = 0.23 \) to \( \beta = 0.33 \) for addition of trifluoroethanol, as the aromatic ring substituent is changed from \( Z = 4-\text{OCH}_3 \) to 4-NMe2. This is consistent with an increase in transition state bonding between the alkane carboxylate base and the transferred alcohol proton (Figure 2A).

Proton transfer from XCH2CH2OH to the carboxylate anion reduces the effective negative charge at the base catalyst and the effective positive charge at the oxygen nucleophile. The latter change is reflected in the decrease in \( \beta_{nuc} \)eff = 0.5 for the uncatalyzed addition of alkyl alcohols to the 1-(4-dimethylaminophenyl)ethyl carbocation to \( \beta_{nuc} \)rel = 0.11 for the addition reaction catalyzed by acetate anion (Figure 3B). These changes in first-derivative effects describe changes, with the changing reaction driving force, in the transition state structure: they define second-derivative effects. The results were modeled on a reaction coordinate profile, which assigns separate axes for bond formation between the alcohol oxygen and benzylic carbon, and for proton transfer from the alcohol...
oxygen to the carboxylate anion,\textsuperscript{17} using a protocol developed by William Jencks that expands upon a model from Bell, Marcus, Hammond, Polanyi, Thornton, and Leffler.\textsuperscript{16}

3. EARLY STUDIES AT BUFFALO

Enzymes achieve rate accelerations through stabilization of their bound transition states by interactions with protein catalysts.\textsuperscript{18−20} The structures of these transition states are of intellectual interest and may guide the development of tight-binding transition state analog enzyme inhibitors, with the potential to function as therapeutic agents.\textsuperscript{21} The first step in β-galactosidase-catalyzed hydrolysis of alkyl β-D-galactopyranosides is transfer of the β-D-galactopyranosyl group from the substrate to the carboxylate side chain of E537 (Figure 4),\textsuperscript{22,23} by a stepwise mechanism where the acidic E461 side chain provides Brønsted catalysis of glycoside bond cleavage to form the β-D-galactopyranosyl cation intermediate,\textsuperscript{24} which is then trapped by the E537 side chain (Figure 4).

The similarity between the transition states for the general base-catalyzed addition of alkyl alcohols to (i) ring-substituted 1-phenylethyl carbocations (Figures 3A and 3B) and (ii) the cation formed at β-galactosidase (Figure 3C) prompted studies to compare the structure-reactivity parameters determined for these enzymatic reactions and the nonenzymatic model.\textsuperscript{25−27}

Figure 2. (A) The ionization of ring-substituted benzoic acids ((Δ\(G^\circ\))\textsubscript{n0} n = 0) and phenylacetic acids ((Δ\(G^\circ\))\textsubscript{X} n = 1). (B) Addition of substituted ethanol to ring-substituted 1-phenylethyl carbocations, with rate constants \(k_X\) (M\(^{-1}\) s\(^{-1}\)), to form protonated alkyl 1-phenylethyl ethers and general-base catalysis by alkane carboxylate anions of nucleophile addition, with rate constants \(k_{YAc}\) (M\(^{-2}\) s\(^{-1}\)), to form ring-substituted alkyl 1-phenylethyl ethers.

Scheme 1. Transfer of a Phosphoryl Group from Phosphorylated Pyridine to 3-Substituted Quinuclidines in Water

Figures 5A and 5B (●) show Brønsted plots of \(\log k_X/k_0\) and \(\log k_{ROH}\) against alcohol \(pK_a\), with slopes of \(\beta_{lg} = -0.75\) and \(\beta_{nuc} = -0.19\), respectively, for reversible β-galactosidase-catalyzed cleavage of alkyl β-galactopyranosides to form the alkyl alcohol and covalent reaction intermediate (Figure 4).\textsuperscript{25,26} Figure 5C shows the plot of equilibrium constants \(\log K_{eq} = \log[k_{cat}/K_m]/(k_{ROH})\), with slope \(\beta_{eq} = -0.75 - (-0.19) = -0.56\) for the β-D-galactopyranosyl group transfer from alkyl β-galactopyranosides to the enzyme.\textsuperscript{25} The large negative \(\beta_{eq}\) of −0.56 shows that interactions between electron-withdrawing alkoxy substituents −X and the electron deficient β-D-galactopyranosyl group or the reactant are destabilizing, compared to the interactions between these −X and the proton of the alcohol product. It is consistent with a sugar substituent that imparts an effective positive charge of +0.56 to the alkoxy oxygen relative to the normalized charge of 0.0 at the alcohol product.\textsuperscript{9} The value \((\beta_{nuc})_{obs} = -0.19\) for alcohol addition is consistent with an effective transition state negative charge of −0.19 at the alkoxy oxygen. This is equal to the sum of the contribution of the effective positive charge from the β-D-galactopyranosyl group plus the true formal negative charge at oxygen. The value of \((\beta_{nuc})_{obs}\) underestimates the buildup of the formal negative charge at this oxygen, because stabilizing charge interactions at oxygen are masked [canceled] by destabilizing dipole–dipole interactions between the electron-deficient sugar and electron-deficient substituents at XCH\(_2\)CH\(_2\)OH.
The value of $\beta_{nuc} = -0.19$ for alcohol addition to the glycosyl cation intermediate reflects the balance between bond formation between the alkoxy oxygen and the glycosyl carbon and proton transfer from oxygen to the carboxylate catalyst. It is consistent with a strong coupling of changes in C=O and H=O bonding at the reaction transition state, as was documented for reversibility of the reversible addition of alkyl alcohols to formaldehyde and acetaldehyde. A weaker coupling between these changes in bonding was determined for general base catalysis of alcohol addition to ring-substituted 1-phenylethyl carbocations ($\beta_{nuc} > 0$, Figure 3B), where motion on the reaction coordinate at the transition state is dominated by formation of the C–O bond, with smaller movement of the proton toward the Brønsted base catalyst.

The C-2 hydroxyl of the $\beta$-D-galactopyranosyl cation reaction intermediate stabilizes the transition state for $\beta$-galactosidase-catalyzed addition of trifluoroethanol by 7.6 kcal/mol. This is accompanied by a decrease in $\beta_{nuc}$ for alcohol addition from $\beta_{nuc} = -0.07$ ($\beta$, Figure 5B) to $\beta_{nuc} = -0.19$ (●). The decrease in $\beta_{nuc}$ with increasing stability of the glycosyl cation intermediate, corresponds to an anti-Hammond shift of the transition state toward reactants, in contrast to the Hammond-type in the shift in the transition state observed for alcohol addition to ring-substituted $\beta$-galactopyranosyl cation intermediate. These differences in coupling observed for general base catalysis of alcohol addition to ring-substituted 1-phenylethyl carbocations, compared to formaldehyde and acetaldehyde, were proposed to arise because of changes in the curvature of the energy surface in the region of the saddle point on a two-dimensional reaction coordinate profile. These results are consistent with a similar tight coupling of changes in bonding for addition of XCH$_2$CH$_2$OH to the protein-stabilized sugar carbocation intermediates of reactions catalyzed by $\beta$-galactosidase.
4. ENZYME CATALYSIS AT PROTEIN CAGES

The insight gained from studies on β-galactosidase has helped us to uncover LFERs of kinetic data for other enzymatic reactions. The transition states for decarboxylation catalyzed by oroticidine 5'-monophosphate decarboxylase (OMPDC)\textsuperscript{32,33}, isomerization catalyzed by triosephosphate isomerase (TIM),\textsuperscript{33–35} and hydride transfer catalyzed by glycerol 3-phosphate dehydrogenase (GPDH)\textsuperscript{33,36} show a similar 12 kcal/mol stabilization by interactions with the phosphodianion of the whole substrate (Figure 6). This transition state stabilization is calculated from the ratio of second-order rate constants for the enzyme-catalyzed reactions of whole and phosphodianion truncated substrates: \([-RT \ln((k_{cat}/K_m)_W)/(k_{cat}/K_d)_T] = 12 \pm 1 \text{ kcal/mol}\). In all three cases, the slow enzymatic reaction of the truncated substrate is strongly activated by the substrate piece phosphite dianion. This activation corresponds to a 6–8 kcal/mol stabilization of the transition states for reactions of truncated substrates by enzyme-bound phosphite dianion.

The 12 kcal/mol stabilization of these enzymatic transition states by interactions with the substrate phosphodianion shows the power of this small fragment to promote efficient enzymatic catalysis. The large fraction of these interactions specifically expressed at these transition states shows that TIM, OMPDC, and GPDH have evolved mechanisms that avoid the full expression of the strong ligand binding at the Michaelis complex, in order to avoid tight and irreversible binding of the substrate.\textsuperscript{20,37,38} The observation of dianion activation of enzyme-catalyzed proton and hydride transfer and decarboxylation reactions is significant because such activation had not previously been considered for these three intensively studied enzymes. This suggests that other exciting results await discovery by mechanistic enzymologists. At the very least, these results are the tip of the iceberg of enzymatic reactions for which there is a large specificity of nonreacting substrate fragments in the stabilization of the enzymatic transition state.\textsuperscript{39}

The similarity in the kinetic results for activation of TIM, OMPDC, and GPDH by phosphite suggested a common mechanism for obtaining dianion specificity for transition state binding. The enzyme X-ray crystal structures provide the critical clue that reveals the mechanism of dianion activation. These structures show that TIM, OMPDC, and GPDH each utilizes phosphodianion binding energy to drive extensive conformational changes that are dominated by the closure of flexible phosphodianion gripper loops over the substrate.\textsuperscript{3,40–44} Loop closure converts flexible open enzymes to closed Michaelis complexes, with the substrate trapped in a protein cage and sequestered from interaction with the solvent water.\textsuperscript{45}

Scheme 2 shows a compelling model for dianion activation. The catalytic activity of the ground-state open form (EO) of these three enzymes is low, compared to the active closed form EC, because the side chains are poorly positioned for catalysis. The enzyme activity toward catalysis of reactions of phosphodianion truncated substrates is likewise low, because only a small fraction of total enzyme is present in the active closed conformation (KC ≪ 1.0), and there is insufficient substrate binding energy to drive the enzyme-activating conformational change. A high activity is observed for phosphorylated substrates and for the reactions of truncated substrates in the presence of phosphite dianion, because of utilization of dianion binding energy to convert these enzymes from inactive EO to active EC.\textsuperscript{20,38,46} Scheme 2 is the induced fit mechanism that was proposed more than 60 years ago,\textsuperscript{47} in another context, and whose significance has since been a subject of debate.\textsuperscript{48} It provides a general mechanism for avoiding the full expression of binding interactions at the ground state Michaelis complex, through the utilization of substrate binding energy to drive formation of closed, high-energy, and catalytically active protein cages, where the number of stabilizing protein–ligand contacts has been optimized.\textsuperscript{38,49} For example, OMPDC-catalyzed decarboxylation of OMP proceeds through a transition state that is stabilized by ca. 31 kcal/mol by interactions with the protein catalyst but with only a modest 8 kcal/mol stabilization of the Michaelis complex to OMP.\textsuperscript{50} Much or all of this 23 kcal/mol difference represents the ligand binding energy utilized to drive the enzyme-activating conformational change from EO to EC.\textsuperscript{41}

We have examined the mechanism for dianion activation in studies of variant enzymes prepared by site-directed mutagenesis. The positions of the active site side chains examined for yeast TIM are shown in Figure 7A for the complex to the phosphoglycolate (PGA) trianion.\textsuperscript{51} Most of these side chains are buried beneath the phosphodianion gripper loop 6 (shaded...
The kinetic parameters $k_{cat}/K_m$ and $k_{cat}/K_{d}$ for catalysis of the reaction of the whole substrate and phosphite dianion (Scheme 3) were determined for catalysis by TIM. We first focused on rationalizing the effects of individual mutations on these rate constants $k_{cat}/K_m$ and $k_{cat}/K_{d}$ by these substitutions. There is a roughly constant difference of $\Delta \Delta G \approx 60 \text{kcal/mol}$ in the activation barriers for TIM-catalyzed reactions of the single whole substrate and phosphite dianion, or the phosphite dianion piece, are utilized to drive transition-state formation for both the whole substrate and truncated substrate (Figures 7A and 7C). The results of a high-level ab initio molecular dynamics (AIMD) computational study show that these transition states have nearly identical barriers to binding and reaction of the single whole substrate and truncated substrate, respectively. The common enzyme conformational change from Michaelis complex to DHAP complex, which shows the full catalytic activity toward deprotonation of enzyme-bound whole and truncated substrates, respectively. This represents the entropic advantage to binding and reaction of the single whole substrate and phosphite dianion, or the phosphite dianion piece, are utilized to drive transition-state formation for both the whole substrate and truncated substrate (Figures 7A and 7C).

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side chains replaced act to directly stabilize the transition states for the respective wild-type enzyme-catalyzed reactions, except for the cationic side chain of K120 from GPDH, which provides electrostatic stabilization of the negative charge that develops at the transition state for enzyme-catalyzed hydride transfer from NADH to DHAP. In the other cases, the side chains function to lock these enzymes into their closed conformations (Eeq), mainly through interactions with the substrate dianion. The near unit slopes for these correlations show that the amino-acid substitutions have nearly the same effect on the stability of the transition states for the enzyme-catalyzed reactions of whole substrates and the substrate pieces and are consistent with the conclusion that Eeq shows nearly the same activity toward catalysis of reactions of whole substrates and the substrate pieces.62–64 As noted above, this is predicted by the model shown in Scheme 2.

We have observed other linear free energy relationships for reactions catalyzed by TIM, OMPDC, and GPDH. For example, third-order rate constants \( k_{cat}/k_{eq}K_X \) (M\(^{-2}\) s\(^{-1}\)) were determined for the activation of GPDH-catalyzed reactions of the truncated substrate glycolaldehyde by fluorophosphate, phosphate and sulfate dianion, and fourth-order rate constants \( k_{cat}/K_KK_{Gua} \) (M\(^{-3}\) s\(^{-1}\)) were determined for the activation of the R269A variant-catalyzed reaction by the combined effects of guanidine cation and each of the above three anions. The excellent LFER between values of log \( k_{cat}/K_KK_{Gua} \) and log \( k_{cat}/K_KK_X \) (not shown) for the reaction of these three dianions, with a slope of 1.0, shows that the R269A substitution does not significantly alter the interaction of these dianions with the enzyme-bound transition state complex, so that the structural integrity of the caged complex is maintained at the R269A variant.63 Figure 9 shows a plot, with a slope of 0.95 and \( r^2 = 0.96 \), for activation of TIM- and GPDH-catalyzed proton and hydride transfer reactions, respectively, by several different tetrahedral dianions. The poor quality of this correlation shows that there are significant differences in the stabilizing interactions of these different dianions at the active sites of TIM and GPDH.

5. TRANSITION STATE ANALOGS

Enzyme catalysts show specificity in binding their transition states with a higher affinity than the substrate. The tight binding observed for analogs of the transition states for enzymatic reactions provides evidence for this proposal. The good linear correlation between values of log \( K_i \) for binding of phosphonoamidate peptide analogs (1) to thermolysin and log \( k_{cat}/K_m \) for thermolysin-catalyzed hydrolysis of the corresponding peptide substrates (2) provides strong evidence that thermolysin stabilizes the covalent tetrahedral reaction intermediate formed by addition of water to the peptide substrate.

![Figure 9. Correlation between third-order rate constants \( k_{cat}/K_KK_X \) (M\(^{-2}\) s\(^{-1}\)) for activation of GPDH and TIM by several tetrahedral dianions.](https://doi.org/10.1021/acs.accounts.1c00147)

![Figure 10. Linear logarithmic correlation between values of \( K_i \) for the breakdown of PGA-TIM complexes (Scheme 4) and \( k_{cat}/K_m \) for isomerization of GAP catalyzed by wild-type TIM from yeast (yTIM) and chicken muscle (cTIM) Trypanosoma brucei (TbbTIM) and by variant forms of these enzymes.](https://doi.org/10.1021/acs.accounts.1c00147)

PGA binds to triosephosphate isomerase (\( K_i \), Scheme 4) with a substantially higher affinity than substrates GAP and DHAP and is a putative analog of the enediolate reaction intermediate (Scheme 4). Figure 10 shows the correlation, with a slope of 0.73 (\( r^2 = 0.96 \)), between values of log \( K_i \) and log \( k_{cat}/K_m \) for the isomerization of GAP catalyzed by wild-type TIM and variants of TIM. This correlation shows that the amino acid side chains substituted for at TIM (Figure 7) act to stabilize the complex between the enzyme and PGA trianion and that ca. 70% of this stabilization is observed at the transition state for substrate deprotonation.

The binding of the PGA trianion to TIM results in an a > 6 unit increase in the p\( K_a \) of the E165 side chain, from p\( K_a = 4 \) at free TIM to p\( K_a > 10 \) at the complex to PGA (Figure 11). This is due to the combined effects of stabilization of the inhibitor complex by a hydrogen bond between the PGA trianion and the protonated E165 side chain and destabilizing electrostatic interactions between the inhibitor trianion and the ionized side chain anion. A similar increase in the p\( K_a \) for this side chain should occur upon proton transfer from the carbon acid substrate to the E165 carboxylate, to form the enediolate anion reaction intermediate (Scheme 5 and Figure 11). The high basicity of the E165 side chain at the complex to the enediolate reaction intermediate analog PGA ([p\( K_a \)COOH: Figure 11] reflects the tight packing of PGA into the solvent-
The activation barrier $\Delta G^\ddagger$ for nonenzymatic deprotonation of the relatively weak carbon acid DHAP ($pK_a \approx 18$) by the weak base propionate anion ($pK_a \approx 5$) is the sum of the thermodynamic reaction barrier $\Delta G^\ominus$ for proton transfer plus the contribution from the intrinsic kinetic reaction barrier $\Lambda$. It is not clear that $\Lambda$ may be reduced for reactions at enzyme active sites compared to water, and attention has been focused on quantifying the reduction in $\Delta G^\ddagger$. EVB calculations to determine $\Delta G^\ddagger$ and $\Delta G^\ominus$ for deprotonation of DHAP bound to wild-type and variant forms of TIM to form the enediolate reaction intermediate give the linear free energy correlation shown in Figure 12, with a slope of 0.74 ($r^2 = 0.99$). The agreement between the computed activation barriers $\Delta G^\ddagger$ and the experimental barriers estimated from $K_{eq}$ for TIM-catalyzed isomerization of GAP is within $\pm 1$ kcal/mol.

The substituted amino acid side chains at TIM (Figure 12) play a role in either maintaining the strong basicity of E165 (I170A, P166A, and L230A) or in the direct stabilization of the enediolate intermediate (K12 and E97). The Bronsted-type correlation shows that these active site side chains function to reduce $\Delta G^\ddagger$ for deprotonation of the weakly acidic $\alpha$-carbonyl carbon acid substrate to form the enediolate phosphate trianion intermediate (Scheme 5) and that ca. 70% of this stabilization is expressed at the transition state for formation of this intermediate and as a decrease in $\Delta G^\ddagger$. These results provide evidence that proton transfer from the substrate to TIM is promoted by placement of active site side chains at positions which impart an optimal basicity to the E165 side chain and optimal stabilization of the negative charge at the reaction intermediate.

7. CONCLUDING REMARKS

The transformation of tables of numerical rate data into graphical LFERs often brings clarity to kinetic analyses. At the very least, these LFERs provide a framework for discussion that may reveal differences in the interpretation and conclusions of studies on reaction mechanisms. These conversations sometimes motivate additional experiments that provide a spark for progress.

The early work on $\beta$-galactosidase-catalyzed glycosyl transfer reactions represented an attempt to extend classical applications of LFERs to studies on enzyme catalysis. Our interest in LFERs then decreased, as the focus of our research shifted to more traditional studies on enzymatic catalysis. However, the opportunities discussed in this Account have resulted in the seamless incorporation of LFERs into analyses of kinetic and computational data pertinent to the effect of active-site directed substitutions on enzyme kinetic parameters. We now understand that LFERs may be observed for kinetic data that correlate the effect of protein substitutions on the rate and/or equilibrium constants for enzymatic reactions, with the caveat that the active-site substitutions are not accompanied by nonspecific changes in protein structure; and note that similar relationships have featured strongly in the work of Fersht and Auerbach. The few examples presented here illustrate the potential of LFERs as tools for the analysis and interpretation of kinetic data for enzymatic reactions. We encourage others to search for additional relationships in their studies on enzymatic reaction mechanisms.
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