PANIC: a 3D dislocation dynamics model for climb and glide in epitaxial films and heterostructures

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Abstract

This paper presents PANIC, a 3D discrete mesoscale dislocation dynamics model which includes a fully quantitative treatment of both dislocation climb and dislocation glide, including climb driven by both osmotic and mechanical stresses and climb enabled by both bulk and pipe diffusion, including full elastic anisotropy for materials with hexagonal symmetry. Efficient calculations can be performed for epitaxial thin films, multilayers and device structures with free surfaces, including those with irregular geometries (e.g. islands). The model also includes the capability to simulate dislocation dynamics during the growth of the thin films or heterostructures. The model has been validated against experiment for thin films of GaN, AlN and AlGaN but is widely applicable to other material systems, both hexagonal and cubic.

Keywords: Dislocation dynamics, Plasticity, Thin films, III-V Semiconductors, GaN

1. Introduction

Dislocations are 1-dimensional line defects whose properties control the mechanical behaviour of many crystalline materials. Their existence was first proposed theoretically in 1934 by Taylor (1934), Orowan (1934a,b,c) and Polanyi (1934), while subsequent studies by Hirsch et al. (1956), Steeds (1973), Cottrell (1963), Hirth and Lothe (1982), and many others described the properties of dislocations, focusing their effects on the plasticity of metals. More recently, research in this area has included atomistic simulations of dislocation core structures (Belabbas et al., 2007).

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Cserti et al., 1992, Fang and Wang, 2000) and dislocation mobilities (Olmsted et al., 2005; Weingarten and Chung, 2013), as well as mesoscopic dislocation dynamics simulations used to model the microstructural development of metals containing high densities of dislocations and subjected to stresses (von Blanckenhagen et al., 2004; Bulatov et al., 2004; Devincre et al., 2011; Ghoniem et al., 2000; Groh et al., 2003; Mordehai et al., 2008; Schwarz, 1999; Weygand et al., 2002; Zbib et al., 2001), and also multi-scale simulations spanning both atomistic and mesoscopic length scales (Bulatov et al., 1998). The majority of these simulations include dislocation glide, the rapid motion of dislocations within their slip plane in response to shear stresses acting across that plane. Dislocation climb can also occur, which is the non-conservative motion of dislocations perpendicular to their glide plane enabled by the diffusion of point defects towards or away from the dislocation core. However, the effects of dislocation climb are complex to calculate and greatly increase computational time. Earlier work includes dislocation climb as a simple ‘drag factor’ (Cai and Bulatov, 2004), and a bulk diffusion climb model has been properly introduced (Ghoniem et al., 2000; Mordehai et al., 2008). A full climb model has also been implemented recently in 2D by Ayas et al. (2014), but this is computationally too expensive for 3D simulations.

The behaviour of dislocations in semiconductors has received considerable attention, particularly in GaN-based materials where heteroepitaxial thin films and devices contain dislocation densities from $10^7$ to $10^9$ cm$^{-3}$. Dislocations in III-nitride devices are known to reduce device lifetimes (Furitsch et al., 2006; Mukai et al., 2006; Tapajna et al., 2011) and efficiencies (Khan et al., 2008; Zhu et al., 2013), as well as increasing leakage currents (Chan et al., 2009; Kaun et al., 2011). However, dislocations also affect the evolution of stresses during device growth. The high mismatch between the lattice parameters, thermal expansion coefficients and elastic constants of the III-nitride films and substrates mean that changes in epilayer composition or growth temperature are usually accompanied by changes in biaxial stresses. This is a major challenge for the growth of GaN-based devices on Si (Dadgar et al., 2000; Haebler et al., 2010; Kroth and Dadgar, 2002; Zhu et al., 2013) and for AlGaN-based devices for ultraviolet light emitters (Amano et al., 1999; Han et al., 2001; McAleese et al., 2004), in which cracking frequently occurs due to the biaxial stresses generated during or after growth. Dopants (such as Si) may also interact with dislocations, further affecting the evolution of stresses during device growth. Previous studies have shown that Si-doping is associated with an increase in tensile stress in the film, but it tends to “pin” dislocations, limiting climb (Forghani et al., 2012; Moram et al., 2011a,b). There also appears to be a range of dislocation-mediated stress relaxation mechanisms in device structures: for instance, misfit dislocations are sometimes ob-
served in In$_x$Ga$_{1-x}$N/GaN structures (Costa et al., 2005), while inclined dislocations (Chang et al., 2010) and “staircase” dislocations (Cherns et al., 2008) dominate in Al$_x$Ga$_{1-x}$N/GaN structures. These devices are based on either c-axis oriented epitaxial films, or (more recently) other ‘nonpolar’ and ‘semipolar’ orientated films. In the former case, dislocation climb is an important mechanism for dislocation mobility (Fu et al., 2011; Moram et al., 2010) as the isotropic in-plane symmetry means that slip systems are rarely activated, despite the presence of high biaxial stresses. In the latter case, the loss of in-plane isotropy enables dislocation glide to occur in response to in-plane biaxial stress (Hsu et al., 2011, 2012). This can lead to extended dislocation segments forming inside the active region of nonpolar or semipolar devices, further reducing device performance.

A large body of literature is devoted to the behaviour of dislocations within III-nitride semiconductor devices but it has not yet been possible to predict the behaviour of dislocations quantitatively. In this work, we present a dislocation dynamics model which enables prediction of the dislocation microstructure in III-nitride films and devices, named PANIC (Parallel ANIsotropic dislocation Climb and glide). This model includes a full treatment of both climb and glide, combining mesoscopic dislocation mechanics with parameters derived from atomistic simulations of dislocation behaviour, and takes into account the effects of the anisotropic elasticity of nitride crystals, the effects of thin film or 3D patterned geometries and the influence of multi-layer image stresses, temperature changes, and the biaxial stresses arising from mismatches in lattice parameters, elastic constants and thermal expansion coefficients between different epilayers and/or the substrate. In short, it includes every parameter that could reasonably be expected to affect dislocation movement in III-nitrides. The model can also be applied to thin film processes including annealing and epitaxial lateral overgrowth (ELOG). Here, we describe the model and validate it by comparison to experimental data on the dislocation microstructure in thin films of GaN and AlGaN.

2. Methods

An overview of the approach used in this model is given in Fig. 1 and is outlined in detail in the following section.

2.1. Simulation supercell

The dislocation dynamics in III-nitride films and multilayers are modelled inside a cuboid anisotropic elastic space, which may include multiple layers of anisotropic elastic media. The dimensions $L_x$ and $L_y$ of the simulation space in the x- and y-
Define a cuboid, laterally periodic, simulation supercell representing a thin film, multilayer or device structure

Define the initial dislocation microstructure within the supercell

Calculate all the forces acting on the dislocations

Elastic ($f_e$)  Self ($f_{self}$)  Image ($f_{img}$)  Misfit ($f_m$)  Osmotic ($f_o$)  Peierls ($f_p$)

Sum up all the forces

Apply mobility functions to convert forces into dislocation velocities

Climb  Glide

Calculate distances moved (if any)

Determine dislocation propagation directions and effects of core reactions

Obtain the final microstructure and point defect density distribution

Add a new layer (‘growth’) according to the new time duration and begin the next time step

Figure 1: Flow chart illustrating the approach used in this discrete dislocation dynamics model.
Table 1: Input parameters required for the dislocation dynamics simulation.

| Parameter                                | Description                                                                 |
|------------------------------------------|-----------------------------------------------------------------------------|
| Atomic volume                           | Includes the vacancy or interstitial formation energy, the diffusion coefficient |
| Growth direction                         | Pre-exponential factor and the self-diffusion energy, the diffusion coefficient |
| Growth rate                             | Pre-exponential factor and the self-diffusion energy, the diffusion coefficient |
| Diffusion coefficients                  | For bulk dilute directions                                                  |
| Temperature                             | Crystallographic orientation of each layer                                  |
| Temperature dependent thermal           | Crystallographic orientation of each layer                                  |
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Equation: \[ \mathbf{z} \cdot \mathbf{n} + \mathbf{\Lambda} (\mathbf{a} \cdot \mathbf{n} + \mathbf{c}) \cdot \mathbf{\eta} + \mathbf{\xi} = [\mathbf{\eta} \cdot \mathbf{\xi}] \]
\[ (hkil) = \frac{h}{a} x + \frac{h + 2k}{\sqrt{3}a} y + \frac{l}{c} z \]  

(2)

To account for semi-polar and non-polar film orientations, where the vector [0001] is no longer aligned with the z-axis, and for some films which may be deposited in a slightly different planar orientation with respect to the substrate, a coordinate orientation transformation is also implemented as described by Hirth and Lothe (1982), by applying a transformation matrix \( T \) to the specific coordinate \( r \), with respect to the three Eulerian angles \( \theta, \phi \) and \( \kappa \) for transformation (see Fig. 2(a)). The stress \( \sigma \), strain \( \epsilon \) and stiffness tensor \( C \) can thus be transformed using the transformation matrix accordingly (Hirth and Lothe, 1982).

2.2. Dislocation modelling

Pure dislocations in the III-nitrides can have any of the three possible Burgers vectors: \( \frac{1}{3} \langle 11\overline{2}0 \rangle \) (a-type), \( \langle 0001 \rangle \) (c-type) and \( \frac{1}{3} \langle 11\overline{2}3 \rangle \) ((a + c)-type). Dislocations are first generated using positions and Burgers vectors assigned randomly using a Mersenne Twister algorithm (Matsumoto and Nishimura, 1998). For a typical simulation, each dislocation has a line vector \( \xi \) which is the same as the normal vector of the substrate plane, although manual setup of dislocation positions and orientations is also possible. The generated dislocations are then divided into small segments defined by positions of the two end nodes, so that segments with the same node are connected together. The minimum length of the dislocation segment is limited by the core radius of the dislocation and the magnitude of the error in the calculated dislocation movement arising from the time integration, while the maximum length is limited by the error related to the angle between two straight segments, which is proportional to the deviation from a long straight segment compared to a curved segment. This discretization allows freedom of movement of the dislocation line in each simulation step. At each time step, the segmentation of the dislocation is adaptively recalculated according to the above criteria and the angle between two segments, thus minimizing the computational power needed, while maintaining an acceptable spatial resolution.

2.3. Forces affecting dislocation movement

In this model, we consider and model the driving forces for the evolution of the dislocation microstructure existing in thin films under realistic growth conditions. At equally spaced points on each dislocation segment, the forces that are important to both glide and climb in multi-layered structures are calculated, including the elastic force, self-force, image force, misfit force, osmotic force and Peierls force. By integrating the points (using Simpson’s rule) on a node’s connected segments
Figure 2: (a) The relationship between the hexagonal and the Cartesian coordinate axes used in this model; (b) The geometric illustration of the Willis-Steeds-Lothe equation (Eqn. 3) and Brown’s equation [Brown 1967]; and geometric setup for (c) collinear field points and (d) field points within the core radius $r_c$ of a dislocation segment.
with respect to a shape function, the segment now acts like it is pinned to the two
nodes at its end points. The total integrated force can then be used to calculate
the actual dislocation movement velocity using an adaptive 4\textsuperscript{th}-5\textsuperscript{th} order Adam-Bashforth-Moulton predictor corrector method (Mathews and Fink, 2006), with the
first 3 time steps being initialized using the Euler-trapezoid method.

2.3.1. Elastic forces

The elastic interactions within and between dislocations are modelled by the
cumulative effect of the computed stress fields from each dislocation on individual
dislocation line segment. The summed stresses lead to an expression for the elastic
force \( f_e \) per unit length \( L \).

The initial method to calculate the stress field of a straight dislocation segment of
finite length is proposed by Brown (1967) as a proof to the theorem of Lothe (1967),
who expressed dislocation forces in terms of energy factors. However, this method
causes singularity in collinear cases, thus we adopted the non-singular expression of
Willis (1970), as described by Yin et al. (2010). This Willis-Steeds-Lothe formula
describes the stress tensor field on a dislocation segment in an infinite anisotropic
elastic space (using the Einstein summation convention):

\[
\sigma_{ij}(r) = \frac{1}{4\pi d} \epsilon_{qln} \beta_{ijkl} C_{pqms} \xi_n \left\{ -m_s Q_{km} + n_s \left[ (nn)^{-1} \cdot (nm) \cdot Q \right]_{km} + n_s \left[ (nn)^{-1} \cdot S^T \right]_{km} \right\}_{BP}^{AP} 
\]

where \( \sigma \) is the stress tensor; \( \epsilon \) is the permutation tensor; \( d \) is the distance \( |CP| \) from
the dislocation line vector to the field point; \( C_{ijkl} \) is the component of the stiffness
tensor \( C(r) \); \( \beta \) is the Burgers vector; \( \xi \) is the dislocation line vector; \( m, n \) and \( \tau \) form
an orthogonal basis as illustrated in Fig. 2(b), with the field point \( P \) (at coordinate
\( r \)) and the line vector \( \xi \) staying on the same plane and \( n \) being this plane’s normal
vector. The term \( (pq)_{jk}^{-1} \), with vectors \( p \) and \( q \), is the Christoffel stiffness tensor given
by \( p_i C_{ijkl} q_j \), and \( (pq)_{jk}^{-1} \) is its inverse. The tensors \( Q \) and \( S^T \) are as determined by
Asaro and Barnett (1974).

To model collinear dislocation segments, the expression becomes (see Fig. 2(c))
(Yin et al., 2010):

\[
\sigma_{kl}(r) = \left( \frac{1}{|BP|} - \frac{1}{|AP|} \right) g_{kl}(\xi) 
\]

where

\[
g_{kl}(\xi) = \frac{1}{8\pi^2} C_{klp} \epsilon_{pqw} \beta_{m} C_{wmrs} \xi_j \int_0^{2\pi} \{ \xi_s (z'z')^{-1} - z_s'(z'z')^{-1} [(\xi z')^{-1} + (z' \xi)] (z'z')^{-1} \}_r \} \mathrm{d} \psi 
\]
The resulting force \( f \) on the original dislocation line segment can be calculated from the stress \( \sigma \) using the Peach-Köhler equation
\[
f = b \cdot \sigma \times \xi.
\]

### 2.3.2. Self-forces

The self-force of a dislocation is the force exerted on a dislocation by itself, which tends to minimise the length of the dislocation and which contains two contributions, the elastic and the core self-force. The elastic self-force is calculated using the same formula as for the collinear dislocation segments (Eqn. 4), but using an inner cutoff radius (Yin et al., 2010) (see Fig. 2(d)). The inner cut-off radius is applied to avoid the singularity arising from classical continuum dislocation theory (Cai et al., 2006) which would lead to a divergence of stress fields computed when the field point is close to the dislocation core. It is usually chosen to be the dislocation core radius. This assumption appears to be reasonable for III-nitrides, as previous critical thickness calculations by Holec et al. (2008) show a good match with experimental data using the core radius as the inner cutoff radius.

The self-force from the core region can be divided into two components: a longitudinal self-force and a torsional self-force (Fitzgerald and Aubry, 2010). The former force will act to reduce the dislocation segment length (thereby minimising its total energy), while the latter force will tend to rotate the segment line direction to a more energetically favourable direction. In an anisotropic elastic space, the core longitudinal force for each dislocation segment is (Fitzgerald and Aubry, 2010):
\[
f^L_c = -\frac{4\pi E_{\text{core}}}{\bar{\mu}} \frac{|b|^2}{2} (b \cdot B \cdot b) \xi
\]
where \( \bar{\mu} \) is the anisotropic shear modulus; \( E_{\text{core}} \) is the core energy; and \( B \) can be calculated by
\[
B_{ij} = \frac{1}{8\pi^2} \int_0^{2\pi} \{(mm)_{ij} - (mn)_{ik}(nn)^{-1}_{kl}(nm)_{lj}\} \, d\psi
\]
And the core torsional force, which tends to rotate the dislocation segments to lower energy configuration, would be (Fitzgerald and Aubry, 2010)
\[
f^T_c = -\frac{4\pi E_{\text{core}}}{\bar{\mu}} \frac{|b|^2}{2} \left[ \left( b \cdot \frac{\partial B}{\partial \phi} \cdot b \right) e_\phi + \left( b \cdot \frac{\partial B}{\partial \theta} \cdot b \right) e_\theta \right]
\]
where \( e_\phi \) and \( e_\theta \) are the base vectors as in a spherical coordinate system.
2.3.3. Image forces

The Willis-Steeds-Lothe formula describes the stress fields of dislocations in an infinite anisotropic elastic space, but surfaces and interfaces play a significant role in semiconductor thin films by imposing 'image forces' on the dislocations (Hirth and Lothe, 1982). Expressions already exist for the stress field of a semi-infinite straight dislocation with arbitrary Burgers vector and angle of incidence, terminating at the free surface of an elastically anisotropic semi-infinite solid (Head 1953b, Yoffe 1961, Lothe et al. 1982). However, to calculate image forces for an arbitrary dislocation microstructure with multiple interfaces, we follow the superposition approach (Fivel et al. 1998, Van der Giessen and Needleman 1995, Yasin et al. 2001), in which the calculation is decomposed into two separate elastic problems: (1) the problem of interacting dislocations in a homogeneous infinite elastic solid, and (2) a dislocation-free version of the original problem. To account for dislocation-boundary (surface) intersection, the dislocation segment that terminates on the surface is extended up to 1000 times the original segment, producing the 'augmented dislocation configuration' (Deng et al. 2008, Weinberger et al. 2009).

We have therefore used a hybrid finite element method combining the method of superposition of multiple subdomains of Zbib and Diáez de la Rubia (2002) with the virtual segment approach of Weinberger et al. (2009). This provides the flexibility to simulate arbitrary interfaces and surfaces and also has an acceptable accuracy provided that the finite element 'mesh' is fine enough near the dislocation-surface interception point.

To implement this approach, each anisotropic elastic layer is treated separately to satisfy a traction-matching condition at the interfaces. The traction force resulting from the image stress \( \mathbf{T}_i \) at the interface between the \( i \)th and \( (i+1) \)th layer is estimated according to:

\[
\mathbf{T}_i = \mathbf{T}_i^\infty \gamma T \]

\( \mathbf{T} = \sigma \cdot \mathbf{n} \); \( \mathbf{T}_i^\infty \) is the traction force on the interface in an infinite anisotropic elastic space such that the resulting traction force \( \mathbf{T}_i = \mathbf{T}_i^\infty + \mathbf{T}_i' \); and \( \gamma = \frac{\mu_{i+1} - \mu_i}{\mu_{i+1} + \mu_i} \). The resulting traction force at the surface with normal \( \mathbf{n} \) would be reduced to zero for a traction-free condition with \( \gamma = -1 \), that is, the image traction force would be a 'reverse' of that in the infinite anisotropic elastic space. It is also obvious that there would be no imaging traction force when layer \( i \) and layer \( i+1 \) are the same, causing \( \gamma = 0 \).

Setting \( \mathbf{T}_i \) as the boundary condition of the finite element calculation, the image stress tensor field can be solved using an external 3D finite element mesh generator \textit{gmsh} (Geuzaine and Remacle 2009) and solver \textit{getdp} (Dular et al. 1998).
image force is most intense near surface and interfaces, the mesh is generated such that it is adaptively meshed finely where the dislocation segments intercept with the interfaces and surfaces (Fig. 3). The image stress, when summed with the stress field in infinite anisotropic elastic space as calculated using the Willis-Steeds-Lothe equation, can satisfy both the traction-matching condition at the interfaces and the traction-free condition at the surface. The Willis-Steeds-Lothe equation (originally formulated for an infinite anisotropic space) is thus adapted to compute the stress field of a dislocation in a finite anisotropic space.

2.3.4. Misfit forces

The misfit force arises from the elastic stress generated by the lattice mismatch between film and substrate. To take into account the effect of the stress tensor field from other factors on the misfit force, the lattice parameters on each layer are recalculated every time step from the total stress field excluding the misfit force itself. In this case, the misfit strain $\epsilon_m(t, T)$ on any layer would be

$$\epsilon_m(t, T) = \frac{a'_f(t, T) - a_f(T)}{a_f(T)}$$ (10)

where $a'_f(t, T)$ is the recalculated lattice parameter at time $t$ and temperature $T$; and $a_f(T)$ is the thermally expanded lattice parameters for the film. Note that Equation (10) follows the convention that compressive strain is negative, and vice
versa. The thermal expansion coefficients $\alpha(T)$ are determined using the Reeber model for GaN and AlN \cite{Reeber2000} and the Suzuki model for InN \cite{Wang2001}, respectively.

Assuming the lattice parameter of the film is lattice-matched to the substrate at time $t = 0$, i.e., $a_f'(0, T) = a_s(T)$, then at this time this equation reduces to the conventionally defined $\epsilon_m = \frac{a_s - a_f}{a_f}$ \cite{Freund2003}, and the re-calculated lattice parameter at any time $t$ is as follows, where $\epsilon_\parallel$ is the equivalent strain (as calculated from other driving forces) parallel to the direction of $a$ calculated from the strain-displacement equation:

$$a_f'(t, T) = (1 + \epsilon_\parallel)a_s(T) \quad (11)$$

If the film does not have the same crystallographic orientation as the substrate, then the lattice parameters in Eqn. 10 and Eqn. 11 can be replaced by the atomic plane spacing so that the lattice parameters and can be solved in a system of parametric equations. So in this case, $d_f'(0, T) = d_s1(T)$, $d_f'(0, T) = d_s2(T)$, then the following applies, where $d_{hi}$ and $d_{hj}$:

$$a_i^2 = \frac{4}{3} \frac{d_{s1}^2 d_{s2}^2 [l_2(h_1^2 + h_1 k_1 + k_1^2) - l_1^2(h_2^2 + h_2 k_2 + k_2^2)]}{d_{s2}^2 l_2^2 - d_{s1}^2 l_1^2} \quad (12)$$

$$c_i^2 = \frac{d_{s1} d_{s2}^2 [l_2^2(h_1^2 + h_1 k_1 + k_1^2) - l_1^2(h_2^2 + h_2 k_2 + k_2^2)]}{d_{s1}^2(h_1^2 + h_1 k_1 + k_1^2) - d_{s2}^2(h_2^2 + h_2 k_2 + k_2^2)} \quad (13)$$

The misfit stress on a layer can thus be computed by applying a fixed displacement calculated from the corresponding misfit strain on its side wall in a finite element calculation.

\subsection{2.3.5 Thermal forces}

External biaxial stress mainly originates from the different thermal expansion coefficients and growth temperatures of different layers. The thermal expansion coefficients of materials were included in the misfit force as described in the previous section. However, thermal mismatch stress can be incurred by the difference in thermal expansions and growth temperatures, in addition to the thermal mismatch arising from the lattice parameters due to difference in thermal expansion coefficient. The thermal mismatch force in this section simulates thermal effect from layers grown below the simulation environment. Using the thermal expansion function from \cite{Reeber2000} and \cite{Wang2001}, the thermal expansion vector, representing the thermal expansion in 3D, for a $c$-plane layer, would be

$$\alpha(T, T_g) = [\alpha_a(T, T_g), \alpha_a(T, T_g), \alpha_c(T, T_g)] \quad (14)$$
where $T_g$ is the growth temperature of the layer, $T$ is the growth temperature during the current time step.

So for a layer with an arbitrary orientation, by rotating the base vectors $x$, $y$ and $z$ to $c$-plane from that orientation, the corresponding in-plane thermal expansion vector would be:

$$\alpha_i (T, T_g) = \alpha (T, T_g) [x^T_c, y^T_c, 0]$$

(15)

where $x_c$ and $y_c$ are the rotated base vectors. Here we assume that the thermal mismatch is a biaxial stress (acting only in planar direction), thus the expansion vector in the vertical ($z$-) direction is zeroed. The differential thermal expansion vector can then be calculated from:

$$\Delta \alpha_i (T, T_g, i) = \alpha_0 (T, T_g, i) - \alpha (T_g, (i-1))$$

(16)

with $\Delta \alpha_0 = 0$. Unlike the misfit force, the effect of the thermal force, which would only be dependent on the in-plane thermal mismatch, should be cumulative starting from the substrate, since each layer is grown on top of a thermally expanded previous layer. So the resultant thermal strain on the whole structure, assuming no bending, would be

$$[\epsilon_T (t, T)]_j = \sum_{i=0}^{n(t)} \Delta \alpha_{ij} (T, T_g, i)$$

(17)

where $n(t)$ is the total number of layers at time $t$.

The thermal stress and thermal force can then be computed by using a finite element method similar to that for the mismatch stress, but with the fixed displacement calculated from the thermal strain instead.

2.3.6. Osmotic forces

Osmotic forces affect dislocation climb and are generated when a non-equilibrium concentration of point defects arises in the material. This creates a driving force for dislocations to restore equilibrium by the absorption or emission of point defects from the dislocation core (resulting in dislocation climb). The magnitude of the osmotic force is therefore controlled by point defect diffusion, and only contributes to dislocation climb. The point defect concentration field $c_v$ are initialised by assuming that they are initially in equilibrium with dislocations. It is then subjected to bulk diffusion as the dislocations move during the simulation [Hirth and Lothe 1982]:

$$\frac{\partial c_v}{\partial t} = D \Delta c_v$$

(18)
where $D$ is the diffusivity. The diffusion of the vacancy concentration is implemented with a finite difference method (FDM) using a 3D forward time, centered space (FTCS) scheme with adaptive time stepping. Section 2.4.2 then describes how the bulk vacancy concentration field is used to approximate climb assisted by pipe diffusion, as according to [Turunen and Lindroos (1974) and Turunen (1976)].

The effect of dislocation climb by both bulk and pipe diffusion on the vacancy concentration field is approximated by absorption (or emission) of point defects in proportion to the length and the distance travelled by a segment of a dislocation. Thus after each iteration of dislocation motion, the vacancy concentration is modified according to the area (in terms of lattice parameters) swept by each climbing dislocation segment. And the osmotic force $f_o$ would be ([Hirth and Lothe 1982]

$$f_o = -\frac{k_BT b_e}{v_a} \ln \frac{c_v}{c_0}$$

(19)

where $k_B$ is the Boltzmann’s constant; $b_e$ is the edge component of Burgers vector; $v_a$ is the atomic volume; and $c_0$ is the equilibrium concentration of vacancies, given by ([Lothe 1960] [Hirth and Lothe 1982]

$$c_0(r) = n_v e^{-\frac{E_f - \sigma(r) \Delta V}{k_B T}}$$

(20)

where $n_v$ is the concentration of possible vacancy site; $\sigma(r)$ is the stress experienced by the material at $r$ causing a change in volume $\Delta V$; and $E_f$ is the vacancy formation energy.

2.3.7. Peierls forces

The Peierls stress affects dislocation glide, acting as an energy barrier due to the varying misfit energy of the dislocation when it glides along a specific slip plane. This lattice frictional force varies with a periodicity closely related to nearest-neighbour interatomic distances within the material and depends on the slip system in which the dislocation lies. The temperature-dependent Peierls force $f_p$ per unit length $L$, which includes the effect of thermal fluctuation at finite temperature, can be calculated by [Chidambarrao et al. (1990) and Srinivasan et al. (2003):

$$f_p = 2\bar{\mu}|\mathbf{b}| \cos \phi \left( \frac{1 - \nu \cos^2 \alpha}{1 - \nu} \omega e \left( \frac{-2\pi d_{hkl}(1-\nu \cos^2 \alpha)\omega}{(1-\nu)|\mathbf{b}|} \right) \right)$$

(21)

where $\phi$ is the angle between the film surface and the normal to the slip plane; $\alpha$ is the angle between the dislocation segment and Burgers vector; $\nu$ is the Poisson’s
ratio; \( d_{hkl} \) is the interplanar spacing of the slip plane \((hkl)\) and \( \omega \) is given by

\[
\omega = e^{-\frac{4\pi^2 n k_b T}{5 \mu V}}
\]  

where \( n \) is the number of atoms per unit cell; and \( V \) is the volume of the unit cell.

2.4. Dislocation mobility

In the model, forces acting on dislocations produce dislocation movement via dislocation mobility functions. These functions convert calculated stresses into realistic simulated glide and climb velocities.

2.4.1. Glide

The simplest dislocation mobility function was proposed by Hirth and Lothe (1982) who used an arbitrary viscous drag coefficient \( B \) to relate the force \( f_g \) per unit length \( L \) and dislocation glide velocity \( v_g \). Mobility function \( M \) (the inverse of \( B \)) has been used in some dislocation dynamics simulations in metals, but a suitable value of \( M \) has not been proposed for nitrides (Cai and Bulatov, 2004). Although an accurate expression exists for \( v_g \) based on the classical theory of kink mobility (Raabe,
several of its variables are unknown. Consequently, recent work has focused on determining $B$ accurately for each material of interest by fitting experimental data or molecular dynamics simulation, resulting in an empirical expression \cite{Fertig2009, Sugiura1997}. We adapt the expression in this work as:

$$v_g = \left[ v_0 \left( \frac{\tau_g}{\tau_0} \right)^m e^{-\frac{Q_g}{k_B T}} \right] (n_g \times \xi)$$ \hspace{1cm} (23)

where $v_g$ is the glide velocity of a dislocation segment; $v_0$ is a constant; $s$ is the slip plane normal; $\tau_g$ is the resolved shear stress acting on the dislocation segment; $\tau_0$ is a constant (1 MPa); and $Q_g$ is the glide activation energy. From experimental data, for GaN was estimated to be 2.0 eV \cite{Sugiura1997} or between 2.0 – 2.7 eV \cite{Yonenaga2003, Yonenaga2003a, Yonenaga2009}; whereas from molecular dynamics simulations, for GaN was estimated to be 1.6 eV, 1.6 eV and 4.7 eV for the basal, prismatic and pyramidal planes, respectively \cite{Weingarten2013}. The estimated glide mobility of III-nitrides is illustrated in Fig. 4.

To account for dislocation glide in the model, the Peach-Köhler force acting on each dislocation segment is resolved in all the possible slip systems described by \cite{Srinivasan2003}. The resolved forces are then compared to the temperature-dependent Peierls forces of the corresponding slip systems. A slip system is designated as active if the net force on it is positive. The final slip direction is then selected according to the largest net glide force.

2.4.2. Climb

It is more complicated to determine an accurate mobility function for dislocation climb. Climb can be driven by both hydrostatic and biaxial stresses and by osmotic effects. Climb is typically limited by the mobility of dislocation jogs \cite{Lothe1960} and can be enabled by bulk diffusion (i.e. diffusion of vacancies or interstitials through the bulk, towards or away from the dislocation) and/or by pipe diffusion (i.e. the preferential diffusion of vacancies or interstitials along the dislocation core). Pipe diffusion is likely to be highly relevant to III-nitride materials, because strong evidence of dislocation climb exists for GaN \cite{Moram2010} and AlN \cite{Fu2011} but both materials have very low vacancy and interstitial self-diffusion coefficients \cite{Laaksonen2009, Terentjevs2010} which are expected to lead to very low bulk climb velocities. Consequently, although a simple mobility function has been used to model the climb velocity $v_c$ \cite{Cai2004}, it cannot capture the complexity of climb processes occurring in real materials. Furthermore, although an expression has been derived for $v_c$ based on the classical theory for bulk climb \cite{Raabe1998}, several of its variables are unknown and it cannot account for
pipe-diffusion-controlled climb. A simpler expression for bulk climb has also been derived (Clouet, 2011), but it is not applicable to pipe-diffusion-controlled climb either. While climb mobility functions were also derived for both bulk and pipe diffusion of a single jog (Lothe, 1960), these assume that climb is driven only by osmotic forces and do not include any contribution from biaxial stress.

In contrast, Turunen has derived a general equation of motion for a climbing, arbitrarily curved dislocation, taking into account both bulk diffusion (Turunen, 1976) and pipe diffusion (Turunen and Lindroos, 1974; Turunen, 1976) along the dislocation core. The climb velocity is described by:

\[
v_c = \left\{ \left( \frac{2\pi V^2 D c_0}{k_B T b_c^2 \ln \frac{R}{\rho}} \right) f_c - \left( \frac{2\nu_0 D \kappa a V^2}{k_B T b_c^2} e^{-\frac{Q_p}{k_B T}} \right) \left[ \frac{b_s}{b_c} \left( \frac{\partial u}{\partial s} \frac{df_c}{ds} + \frac{\partial^2 f_c}{ds^2} \right) \right] \right\} \frac{b \times \xi}{|b \times \xi|} \tag{24}
\]

\(V\) is the vacancy volume; \(f_c\) is the dislocation climb force; \(\nu_0\) is the attempt frequency of atomic jumps; \(Q_p\) is the activation energy of pipe diffusion; \(b_s\) is the screw component of the Burgers vector; \(\kappa\) is a numerical constant (~0.5); \(a\) is the jump distance in the dislocation core; \(R\) is an outer cutoff radius at \(c(r) = c_0(r)\); \(\rho\) represents the dislocation core radius; and \(s\) is a point along the dislocation line. The first term of the equation accounts for climb due to bulk diffusion, while the latter term accounts for climb due to pipe diffusion. The dislocation core is considered as a tunnel along the line direction made up of atomic sites where diffusive jumps could happen. From the climb force \(f_c\) and the activation energy required for a diffusion jump \(Q_p\), the effective number of diffused atoms causing climb of the dislocation segment can be related to the climb force, and thus \(v_c\) can be calculated from the net atomic flux diffusing along the dislocation core. This expression models both bulk and pipe diffusion and contains parameters that can be either measured or computed for III-nitrides, so therefore it is chosen for use in the simulations.

We note that the \(\frac{df_c}{ds}\) in the second term only exists when the dislocation line is not straight, i.e., \(\frac{du}{ds} \neq 0\): this was omitted in the original work based on the assumption that the dislocation has a low curvature (Turunen, 1976), which breaks down based on the simulations. Another point to note is that the Debye frequency, which is the theoretical maximum of the jump frequency, is more readily available from previous studies and is used as a sensible guess of the actual attempt frequency. It is calculated from the Debye temperature given in Table 2 by \(\omega_0 = \frac{k_B \omega_D}{h}\). The Debye temperatures reported for GaN show a wide scatter between 500 K and 900 K and appropriate values have not yet been determined for all III-nitrides. However, the \(I_s\) values used in the fitting of the Varshni formula are closely associated with
the Debye temperatures (Roder et al., 2005; Teisseyre et al., 1994) and are available for all III-nitrides (Vurgaftman and Meyer, 2003), so they have therefore been used in this work.

2.5. Modelling of thin film growth

Typically for nitride semiconductors, the most significant change in dislocation microstructures takes place during the growth of thin films and multilayers. Therefore, a simple growth model is introduced to the dislocation dynamics model, in which the film thickness can increase (or decrease, e.g. during etching) according to a predefined growth rate on each facet on the surface of the film, after which the stress field on dislocations is recalculated at each time step. This approach enables the response of dislocations to the change in film thickness to be modelled.

Complex film structures can then be ‘grown’ during the simulation using multiple ‘growth’ steps with step-specific time durations, the growth rate of the individual facet and material types. A simple growth mechanism is implemented such that the dislocation will choose to elongate along the direction of the substrate normal (usually [0001]) the surface facet that it is closest to, along other common dislocation directions for nitride films, ⟨1120⟩ and ⟨1010⟩, or along the original dislocation line direction, according to the lowest calculated strain energy that will be incurred.

2.6. Choice of parameters used in the model

Table 2 summarises the key material parameters used in the model, with references.

2.6.1. Core radii and core energies

The three types of pure dislocations in III-nitrides are summarised in Table 2. However, approximately 99% of the dislocations found in heteroepitaxial III-nitride structures on sapphire are either \(a\)-type or \((a + c)\)-type (Moram et al., 2009), apart from at the early stages of film growth where different ratios of different dislocation types can occur. Different core structures are possible (Lymperakis et al., 2004), but the commonest are the 5/7-atom ring structure for \(a\)-type dislocations and the 5/6-atom ring structure for the \((a + c)\)-type dislocations (Rhode et al., 2013). Therefore, we have used reliable literature values for the core radii and the core energies of dislocations in III-nitrides with these core structures, as listed in Table 3.

2.6.2. Activation energies for dislocation climb

Even though the precise mechanism of climb is not known in the III-nitrides, the activation energy of the rate-limiting step of the climb process can still be identified
by comparison to experimental data. The model was used to simulate the growth of GaN- and AlN-on-sapphire films according to the conditions reported by [Moram et al. (2010) and Fu et al. (2011)] respectively and average dislocation velocities were obtained. These results were then compared to the average dislocation velocities obtained from the experimental results reported by [Moram et al. (2010) and Fu et al. (2011)] respectively. The upper and lower error bounds are obtained by assuming no and maximum dislocation inclination responsible for the displacement of dislocation. Fig. 5 shows the average dislocation velocities obtained from simulations and plotted

Table 2: Parameters used in simulations of thin films and multilayers of AlN, GaN, InN and their alloys. N.B. The value for \( Q_p \) of InN is currently unknown as the relevant experimental studies are not available in the literature.

| Material parameters | Value(s) chosen | References |
|---------------------|----------------|------------|
| \( C_{11,\text{AlN}} \) | 396 GPa | |
| \( C_{12,\text{AlN}} \) | 137 GPa | |
| \( C_{33,\text{AlN}} \) | 373 GPa | |
| \( C_{11,\text{GaN}} \) | 367 GPa | |
| \( C_{12,\text{GaN}} \) | 135 GPa | |
| \( C_{33,\text{GaN}} \) | 405 GPa | |
| \( C_{11,\text{InN}} \) | 223 GPa | |
| \( C_{12,\text{InN}} \) | 115 GPa | |
| \( C_{33,\text{InN}} \) | 224 GPa | |
| \( a_{\text{AlN}} \) | 3.111 Å | |
| \( c_{\text{AlN}} \) | 4.980 Å | |
| \( a_{\text{GaN}} \) | 3.189 Å | |
| \( c_{\text{GaN}} \) | 5.186 Å | |
| \( a_{\text{InN}} \) | 3.538 Å | |
| \( c_{\text{InN}} \) | 5.706 Å | |
| \( \theta_D \) | 1462 K (AlN) | |
| \quad | 830 K (GaN) | |
| \quad | 624 K (InN) | |
| \( D_B \) | \[ 72.1e^{-\frac{\Delta H}{k_B T}} \] | |
| \( Q_g(\text{AlN}) \) | 3.1 eV | |
| \( Q_g(\text{GaN}) \) | 2.1 eV | |
| \( Q_g(\text{InN}) \) | 1.2 eV | |
| \( Q_p(\text{AlN}) \) | 3.4 eV | |
| \( Q_p(\text{GaN}) \) | 3.7 eV | |
| \( V_A \) | 10.44 Å³ | |
| \( V_{Ga} \) | 11.42 Å³ | |
| \( V_{In} \) | 15.46 Å³ | |

\*includes the vacancy or interstitial formation energy, the diffusion coefficient pre-exponential factor and the self-diffusion enthalpy.
Table 3: Core radii and energies for dislocations in III-nitrides, including \( \alpha \)-type dislocations with 5/7-atom ring cores, and (\( \alpha + c \))-type dislocations with 5/6-atom ring cores from atomistic simulations.

| Material | Burgers vector \( \mathbf{b} \) | Core \( \rho \) (Å) | \( E_{\text{core}} \) (eV Å\(^{-1}\)) | Method | Reference |
|----------|--------------------------------|-----------------|------------------|--------|----------|
| GaN      | \( (\alpha + c) \)-type       | 7.2             | 3.12             | MSW potential | Belabbas et al. (2007) |
|          | \( \alpha \)-type             | 7.0             | 1.57             | Multiscale DFT with SW potential | Lymperakis (2005) |
| AlN      | \( \alpha \)-type             | 6.0             | 1.61             | Many body | Kioseoglou et al. (2009) |
| InN      | \( \alpha \)-type             | 8.3             | 1.71             | Many body | Kioseoglou et al. (2009) |
|          |                                | 5.4             | 1.66             | Many body | Kioseoglou et al. (2009) |

against different pipe diffusion activation energies for GaN films (each simulation was repeated 10 times; results for AlN were very similar). A small change in \( Q_P \) alters the dislocation climb velocities by orders of magnitude, while the simulated climb velocity is much less sensitive to the other simulation parameters. This is as expected considering Eqn. 24 for climb mobility, where the climb velocity is exponentially dependent on the activation energy. From Fig. 5, \( Q_P \) for AlN and GaN are thus found to be approximately 3.4±0.45 eV and 3.7±0.40 eV respectively. However, the average climb dislocation velocity estimated from experiment shows that dislocations climb faster in AlN than in GaN, so AlN has a lower pipe diffusion activation energy. The difference in pipe diffusion activation energies between GaN and AlN may be due to relative size effects: the atomic radius of Al is approximately 6% smaller than that of Ga (135 pm and 143 pm, respectively) (Rhode et al. 2013), whereas the lattice parameters and consequently the internal diameters of the dislocation cores are only 2.5% smaller for AlN than for GaN (\( a_{\text{AlN}} = 3.111 \) Å and \( a_{\text{GaN}} = 3.189 \) Å) (Moram and Vickers 2009). In the simulations, the rate of diffusion is proportional to \( e^{-Q_{P}/k_B T} \) and to the cross sectional area of the dislocation pipe \( \pi r_c \), a decrease in activation energy with increasing relative core radius \( r_c \) is expected.

3. Results

The simulations were validated by comparison to transmission electron microscopy data of an AlN epilayer on a sapphire substrate and of an Al\(_{0.87}\)Ga\(_{0.13}\)N film on an AlN-on-sapphire substrate. For the AlN film on sapphire, the simulation was set up using a simulation cell with a lateral size of 169 nm × 169 nm containing 10 dislocations with randomly assigned Burgers vector directions and with types as-
Figure 5: Average dislocation velocities plotted versus pipe diffusion activation energy, subjected to different external biaxial stresses. Experimental data for GaN and AlN are extracted from the results of Moram et al. (2010) (solid orange line) and Fu et al. (2011) (dashed greenish blue line), respectively. Their error ranges are represented by the dotted lines with light orange colour for GaN and light greenish blue colour for AlN.

signed randomly according to the proportions found experimentally. In this case, the simulations included three $a$-type dislocations, six $c$-type dislocations and one $(a + c)$-type dislocation, as these ratios are in proportion to the amounts of different types of dislocations found experimentally at the very early stages of film growth [Fu et al., 2011] (note that the proportion of $a$-type dislocations rises greatly as the film thickness increases, because $c$-type dislocations tend to annihilate each other easily during the initial stages of film growth [Fu et al., 2011]. All other settings were based on experimental growth parameters, including an epilayer growth temperature of 1403 K and a growth rate of 1.3 $\mu$m hr$^{-1}$. Here, a free surface was defined at the bottom of the AlN film to simulate the effects of the disordered nucleation layer found experimentally between AlN films and sapphire substrates. The effects of the experimentally verified sapphire substrate miscut of 0.25° towards the $[11\bar{2}0]$ direction were tested by performing one simulation including the miscut and one simulation without it.

For the Al$_{0.87}$Ga$_{0.13}$N film on AlN, the simulation was set up using a simulation cell with a lateral size of 396 nm $\times$ 396 nm containing 10 dislocations with randomly
assigned Burgers vector directions and with types assigned randomly according to the proportions found experimentally, in this case nine $a$-type dislocations and one $(a + c)$-type dislocation. All other settings were based on experimental growth parameters, including an epilayer growth temperature of 1382 K and a growth rate of 2 $\mu$m hr$^{-1}$. The interface is a continuum boundary and the simulations were initiated assuming that the pre-existing dislocations in the AlN layer (beneath the AlGaN film) were initially straight and aligned along [0001].

Figure 6: (a) Simulation of an AlN film grown on sapphire with a substrate miscut of 0.25° towards [1120]; (b) cross-sectional weak-beam dark field transmission electron micrograph of a 1 $\mu$m thick AlN film grown on a sapphire substrate, with a substrate miscut of $0.25 \pm 0.10°$ towards [1120]. The micrograph was taken in the $g(5g)$ condition with $g = 1120$, revealing $a$-type and $(a + c)$-type dislocations. The plane of the TEM foil and the plane on which the contents of the simulation cell are projected is (1010). Different colours are used for each dislocation in the simulation, for ease of identification. The upper and lower dashed lines in (b) correspond to the vertical boundaries of the simulation as in (a).

Fig. 6 shows the simulation results and the corresponding experimentally determined microstructure for the AlN film on sapphire. The colours of the dislocations in the figure represent their corresponding Burgers vectors ($b_x$, $b_y$ and $b_z$ are mapped to red, green and blue colours, respectively). No dislocation bending is predicted in simulations of the growth of AlN on sapphire without any miscut: all dislocations remain oriented parallel to [0001]. However, when a substrate miscut is included in the simulations, the model reproduces accurately the effects of the miscut on the microstructure of the AlN films. For example, the substrate miscut of 0.25° towards [1120] results in the onset of dislocation bending away from [0001] at an AlN thickness of approximately 150 nm, consistent with experimental data. These data indicate that the substrate miscut has an important role to play in inducing disloca-
tion bending, which is well known to result in an increase in dislocation annihilation and reduction with increasing epilayer thickness in III-nitride films.

Fig. 7 shows the simulation results and the corresponding experimentally determined microstructure for the Al\textsubscript{0.87}Ga\textsubscript{0.13}N/AlN heterostructure. The average (projected) dislocation bending angle away from [0001] in the TEM specimen was 6.7° ± 1.4°, whereas the projected dislocation bending angle away from [0001] from the simulations was 6.7° ± 0.6°, i.e. the same, within the standard error. Minor differences may relate to the fact that the image force from the AlN/sapphire interface was not included in this simulation to minimise computational expense, as the microstructure was expected to be dominated by the effects of misfit stresses at the Al\textsubscript{0.87}Ga\textsubscript{0.13}N/AlN interface. The simulations match the experimental microstructure accurately and are consistent with the low experimentally observed strain relaxation of 6%. These results are in contrast to widely cited equilibrium critical thickness calculations for the Al\textsubscript{x}Ga\textsubscript{1-x}N/AlN system (equivalent to the inverse of the Al\textsubscript{x}Ga\textsubscript{1-x}N/GaN calculations), which predict incorrectly that stress relaxation should occur by dislocation glide at an Al\textsubscript{0.87}Ga\textsubscript{0.13}N thickness of just 80 nm (Holec et al., 2008). The discrepancy occurs because the equilibrium critical thickness calculations assume that dislocation glide is the only stress relief mechanism that can act in these heterostructures, whereas our model includes the effects of dislocation climb, of image stresses and of the influence of neighbouring dislocations (each with their own strain field). This result indicates that dislocation climb plays an important role in stress relaxation in AlGaN-based heterostructures. The effects of dislocation climb on critical thicknesses for stress relaxation will be explored further in a subsequent publication.

4. Discussions

Table 4 shows a list of 3D discrete dislocation dynamics simulation packages, including this model. A comparison of our model considering the crucial features for simulating dislocation dynamics in thin film nitride semiconductors is also presented. Most of the newer packages have incorporated elastic anisotropy, although only microMegas has explicitly stated and demonstrated the ability to handle hexagonal crystals (Monnet et al., 2004). Most of the packages have been used to study strained epitaxial films with a heterointerface terminated by a free surface, although only MDDP (Zbib and Díaz de la Rubia, 2002) and PDD (Ghoniem and Han, 2005) have demonstrated the ability to handle multilayered structures (i.e. those containing more than two layers). However, most of these studies focus on the "\textit{channeling stress}", that is, the thickness-dependent critical stress driving a threading dislocation
to introduce a misfit segment. Realistic misfit stresses are much less studied and data appear only for metallic heterointerfaces (Groh et al., 2003), rather than for semiconductors. Therefore, the key advantage of the present approach is the successful implementation and combination of the following features:

i. The ability to handle both climb and glide, including climb driven by both osmotic and mechanical stresses and enabled by both bulk and pipe diffusion.

ii. Full elastic anisotropy for materials with hexagonal symmetry.

iii. Efficient calculations for thin film multilayers and free surfaces, including irregular geometries (e.g., islanded layers), using a superposition method (Tan and Sun, 2006).

iv. Ability to simulate dislocation dynamics under different thin film growth conditions, including the effects of changes in growth temperature between different layers in a heterostructure.

5. Conclusions

In this work we have described PANIC, a new model for discrete dislocation dynamics simulations which uses an adaptive multi-scale meshing approach combined
| Simulation code | Discretization | Stress calculation | Anisotropy | hcp | Free surface | Multi-layer | Misfit forces | Climb | References |
|----------------|----------------|-------------------|------------|----|--------------|-------------|--------------|-------|------------|
| This model     | Straight line  | Willis-Steeds-Lothe | Yes        | Yes| Yes          | Yes         | Yes          | Yes   | (bulk and pipe) |
| K-D            | Edge-screw     | Brown             | Yes (line tension) | Yes | Bilayer      | Yes         |              |       | Brown [1964]; Groh et al. [2003] |
| MDDP           | Straight line  | Simple dislocation bend | Yes | Yes | Yes         |             |              |       | Zbib et al. [2001]; Zbib and Díaz de la Rubia [2002]; Akshleh et al. [2007] |
| microMega      | Straight line  | Modified de Wit    | Yes        | Yes| Yes          |             |              |       | Devincre [1995]; Monnet et al. [2004]; Devincre et al. [2011] |
| ParaDis        | Straight line  | Willis-Steeds-Lothe | Yes        | Yes|             |              | Yes (glide-like mobility law) |       | Bulatov et al. [2004]; Cai and Bulatov [2004]; Mejíe et al. [2006]; Arsenlis et al. [2007]; Yin et al. [2010] |
| PARANOID       | Tracking points| Modified Brown    | Yes        | Yes| Bilayer      | Yes         |              |       | Schwarz and Tersoff [1996]; Schwarz [1999]; Liu and Schwarz [2005] |
| PDD            | Cubic spline   | Han and Ghoniem   | Yes        | Yes| Yes (planar films) | Yes         | Yes (bulk) |       | Ghoniem et al. [2000]; Han et al. [2003]; Ghoniem and Han [2005] |
| Tridis         | Edge-screw     | Modified de Wit    | Yes        | Yes|             | Yes (bulk)  |              |       | Devincre [1995]; Hartmaier et al. [1999]; Mordehai et al. [2008] |
| VGA            | Tracking points| Modified Brown    | No         | Yes| Bilayer      | Yes         |              |       | Schwarz [1999]; von Blanckenhagen et al. [2001, 2004] |
| W              | Straight line  | Brown             | Yes        |     |              |             |              |       | Brown [1964]; Weygand et al. [2002] |

Table 4: A list of 3D discrete dislocation dynamics simulation packages available currently, including features that are either published or explicitly described in the corresponding model’s description in the accompanying manual or on the relevant host website.
with input from atomistic simulations to reproduce mesoscale dislocation behaviour. This code can accommodate both hexagonal and cubic materials and includes the full effects of elastic anisotropy. Multilayer structures can be simulated, including the effects of multiple free surfaces and interfaces. Misfit forces and thermal stresses can be included, while arbitrary geometries (both planar and non-planar) can also be simulated. This code has been validated for the case of technologically important AlN and AlGaN-based thin film heterostructures, for which simulation code inputs are well known. This is the first dislocation dynamics simulation to accurately model dislocation behaviour within semiconductor heterostructures: it is therefore anticipated that the code will facilitate the design and development of devices including defect-containing heterostructures, especially for the challenging III-nitride materials system.

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