Strong 1D localization and highly anisotropic electron–hole masses in heavy-halogen functionalized graphenes†

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While halogenation of graphene presents a fascinating avenue to the construction of a chemically and physically diverse class of systems, their application in photovoltaics has been hindered by often prohibitively large optical gaps. Herein we study the effects of partial bromination and chlorination on the structure and optoelectronic properties of both graphane and fluorographene. We find brominated and chlorinated fluorographene derivatives to be as stable as graphane with a detailed investigation of the systems band structure revealing significant 1D localization of the charge carriers as well as strongly electron–hole asymmetric effective masses. Lastly using $G_0W_0$ and BSE, we investigate the optical adsorption spectra of the aforementioned materials whose first adsorption peak is shown to lie close to the optimal peak position for photovoltaic applications ($\approx 1.5$ eV).

I. Introduction

The need for clean and sustainable energy has become one of the main driving forces of scientific research in the 21st century. Amongst the large number of proposed solutions to the energy crisis, solar cell technology has received a great amount of attention promising to replace large parts of fossil-fuel based energy production in the future. For this to be realized though, the availability of cheap and efficient solar cell materials is of great importance. While classical solar cells are mainly based on silicon, 2D materials, notably graphene1–5 and MoS2 6–9 have recently emerged as possible alternatives, allowing for the construction of ultrathin photovoltaic devices.10

Though graphene itself has sparked the interest of the photovoltaic community, its chemical modifications, most prominently its fully hydrogenated form (graphane11,12) and its fully fluorinated form (fluorographene13,14), have not yet found applications in solar cell technology due to their prohibitively large optical gaps.15–17 Another problem plaguing all possible applications of 2D materials in solar cells is the presence of strongly bound electron–hole pairs (excitons) created upon optical excitation.18,19 To achieve large photocurrents the electron–hole pairs should be easily separable which makes the application of 2D materials to solar cells challenging.

Herein we present a possible solution to both the aforementioned problems via the introduction of heavy halogen atoms into graphane and fluorographene. While, as we will show, these modifications help to significantly redshift the optical adsorption of the aforementioned materials, the strong asymmetry in their charge-carrier masses could be exploited to overcome the problem of strong exciton binding, allowing for an efficient separation of electron–hole pairs and in turn high quantum yields in future solar cells. We will consider in detail some of the main properties required for a viable solar cell i.e. its stability, optical adsorption spectrum and exciton binding energy using single particle methods (DFT) as well as many-body methods i.e. $GW^{20}$ and the Bethe–Salpeter equation (BSE),21 to accurately account for both electron–electron as well as electron–hole interactions.

Our study is based on earlier work performed by Karlicky, Zbořil and Otyepka22 though we extend on the structures proposed by them and take a more in-depth look at the systems structural, electronic as well as optical properties. The systems are based on 1 × 2 supercells of graphane and fluorographene in which every second row of H/F atoms along the zigzag direction has been substituted by Br/Cl and we considered both symmetric as well as asymmetric substitutions and functionalization on only one of the two faces of the graphane/fluorographene layer.

II. Computational details

Structure optimizations on all systems were performed using the CRYSTAL14 program23,24 together with the M06-2X25 functional using the POB-triple-$\zeta$ basis set proposed by Peintinger et al.26
In the case of Br and Cl, HSE06\textsuperscript{27–30} band gap calculations on the relaxed structures were done employing the Stuttgart triple-z\textsubscript{2} basis set as modified for use in periodic calculations by Steenbergen et al.,\textsuperscript{31} together with the associated quasirelativistic pseudopotentials.\textsuperscript{12,31} For C, F and H\textsubscript{2} basis sets were constructed according to the procedure described by Usyniv.\textsuperscript{32} In all cases the description of the vacuum region was enhanced by adding ghost atoms containing a 1 s function with an exponent of 0.06 \textit{a} \textsubscript{0}, 1 \textit{Å} above the position of the halogen atoms.

Using the obtained structures we performed electronic structure calculations using the GPAW\textsuperscript{35–37} code. It is well known that DFT alone is unable to accurately describe electron–electron interactions which results in a systematic underestimation of the band gap. To remedy this issue we performed \( G_0W_0 \) calculations based on our DFT results which provides a first-principles description of electron correlation resulting in a significant improvement in the accuracy of the band gap.\textsuperscript{20,38–41} Still, \( G_0W_0 \) band gaps only allow one to calculate a system’s quasiparticle gap, i.e. the difference between the ionization potential and electron affinity. This leaves out interactions in electron–hole pairs created when a system is excited through the adsorption of light. These effects are of particular importance in low-dimensional systems where the screening of the electron–hole Coulomb interaction is significantly reduced as compared to the 3D case.\textsuperscript{18,19,42,43} To account for both electron–electron as well as electron–hole interactions we therefore employed the BSE method\textsuperscript{21,42,44} on top of our \( G_0W_0 \) results. BSE is able to account for excitonic effects missing in the \( G_0W_0 \) treatment and we use it to calculate the adsorption spectrum of our systems in the optical limit (\( q \rightarrow 0 \)) which is given by the imaginary part of the frequency dependent dielectric function. Both \( GW \)\textsuperscript{45–47} and BSE\textsuperscript{48,49} calculations have been widely and successfully applied to study the optical properties of materials.

Given the cost of the \( G_0W_0 \) calculations at the dense k-grids needed for well-converged BSE results, BSE calculations following \( G_0W_0 \) were performed employing the scissor approximation i.e. shifting the unoccupied DFT bands by the energy difference between the DFT and \( G_0W_0 \) gap. To avoid confusion, BSE calculations based on DFT orbitals where the unoccupied states have been shifted to reproduce the \( G_0W_0 \) gap will be labeled with the superscript \( G_0W_0 \) e.g. BSE@\text{GLLB-SC}\textsuperscript{\textit{G0W0}}. We tested the validity of this approach for two smaller (1 × 1) test systems and found results of full BSE@\text{G0W0} calculations to agree to within 0.05 eV with those obtained by applying the scissor approximation.

Lastly, as will be seen later, the PBE\textsuperscript{50} functional severely underestimates band gaps for the systems considered herein and, as we suspect, for systems containing strongly localized electrons in general. It therefore provides a poor starting-point for \( G_0W_0 \) calculations which assume the DFT one-particle wavefunctions to be close to the true quasiparticle wavefunctions. A possible solution consists in the use of screened hybrid functionals (e.g. HSE03/HSE06) as a starting point for \( G_0W_0 \) and this approach has already been successfully applied to a number of systems in the literature.\textsuperscript{16,51} Such calculations are though quite costly computationally as compared to GGA calculations and quickly become prohibitively expensive for larger systems. To circumvent these problems we investigated a low-cost alternative to hybrid functional calculations using the \text{GLLB-SC} functional\textsuperscript{52} which provides a computationally efficient approximation to the EXX-OEP, resulting in a better description of the electronic ground state for the case of highly localized systems.

The \text{GLLB-SC} functional can further be used to calculate the quasiparticle band gap of an N-electron system i.e. the difference of the ionization potential and electron affinity as the sum of the Kohn–Sham gap and the derivative discontinuity.\textsuperscript{52,53} This approach has been shown to give band gaps in excellent agreement with experimental results\textsuperscript{54} at a computational cost close to that of GGA. \text{GLLB-SC} + \( A_{xc} \) gaps would therefore seem the ideal starting point for subsequent \( G_0W_0 \) calculations. As pointed out by Yan et al.\textsuperscript{44} though inclusion of the derivative discontinuity in the calculation of the dielectric constant at the RPA level, i.e. excluding electron–hole interactions, leads to a systematic underestimation of static screening. Yan et al. focused on BSE calculations where they showed BSE based on \text{GLLB-SC} + \( A_{xc} \) orbitals and eigenvalues performed better when excluding the derivative discontinuity in the calculation of the dielectric constant. Still the same is not necessarily true for BSE@\text{G0W0} using \text{GLLB-SC} as a starting point. While an underestimation of the dielectric constant at the \( G_0W_0 \) level does lead to an increase in the quasiparticle gap, this in turn will result in decreased screening at the BSE level, increasing the exciton binding energy and thereby redshifting the position of the first excitation peak.\textsuperscript{18,42}

Given this uncertainty with regards to the best computational method, we have opted to provide results both including and excluding the derivative discontinuity (i.e. \( G_0W_0@\text{GLLBSC} \) and \( G_0W_0@\text{GLLB-SC} + A_{xc} \)). As we will see later, while results are obviously different, the particular choice of computational method does not influence our overall conclusions.

### III. Results and discussion

**A. Structural properties and stability**

We mentioned in the introduction that, while some of the structures considered in this work were originally proposed by Karlický et al.,\textsuperscript{22} others have, to the best of our knowledge, never been studied before. We will therefore begin our discussion by briefly laying out the systems as well as discuss their predicted stability compared to better-known graphene halides.

Fig. 1 shows a schematic representation of all the systems considered in this work as structurally optimized using the M06-2X functional. Comparative structure-relaxations using the PBE functional resulted in only slight differences (see ESI†). While the initial study by Karlický et al. considered only single unit cells for the pure Br systems (BrFBr and BrHBr) our investigation on 1 × 2 supercells showed the systems to undergo significant buckling of the bromine atoms. This deformation is indicated for the case of BrF, BrFBr and BrFCl in Fig. 1. It results in a notable increase in the band gap, e.g. while the BrFBr gap is equal to \( \approx 0.85 \) eV at the \text{GLLB-SC} + \( A_{xc} \) level if no buckling of the
bromines is allowed, the gap increases to 1.52 eV after relaxation in the supercell. This increase is likely caused by the dealignment of the bromine atoms which dominate the systems valence band maximum (VBM). It is consequently stronger in BrFBr as compared to BrFCl where buckling causes an increase in the band gap of ≈0.5 eV (going from 0.75 to 1.24 eV) as compared to the BrFBr increase of ≈0.7 eV. This difference is in line with the increase in the Br–C–C–Br dihedral angle from 9.6° to 10.7° as shown in Fig. 1 leading us to believe that it is in fact a dealignment between the Br atoms causing the increase in the band gap.

In order to verify the stability of the systems shown in Fig. 1, we calculated reaction energies starting from graphane (GrH), fluorographene (GrF) as well as chlorographene (GrCl) and bromographene (GrBr) and the hydrogen/halogen molecules \( \text{H}_2, \text{F}_2, \text{Cl}_2 \) and \( \text{Br}_2 \) as \( E_{\text{stab}} = (E_{\text{prod}} - E_{\text{react}})/N_C \) with \( N_C \) being the number of carbon atoms in the system, in analogy to the method used by Karlický et al. \(^2\)

While only M06-2X results are shown in Table 1, PBE provides very similar numbers and results are given in the ESL. \(^6\) We see that all systems are more stable than GrCl with fluorographene-based systems (BrFF, BrFBr and BrFCl) being more stable than their graphane-based counterparts (BrHH, BrHBr and BrHCl).

Table 1 Stability of the compounds considered in this work as calculated at the M06-2X level. All values in kJ mol\(^{-1}\) normalized to the number of carbon atoms in the unit cell. For comparison the M06-2X stabilities of GrF, GrCl and GrBr relative to GrH are \(-172 \text{ kJ mol}^{-1}\), \(-136 \text{ kJ mol}^{-1}\) and \(-245 \text{ kJ mol}^{-1}\) respectively.

|     | GrH | GrF  | GrCl  | GrBr  |
|-----|-----|------|-------|-------|
| BrFF| −67 | 105  | −203  | −311  |
| BrFBr| 18  | 189  | −119  | −227  |
| BrFCl| −4  | 167  | −141  | −249  |
| BrHH| 43  | 214  | −93   | −202  |
| BrHBr| 69  | 240  | −68   | −176  |
| BrHCl| 49  | 220  | −88   | −196  |

BrFCl and BrFF in particular are predicted to be more stable than even GrH and BrHBr’s stability, though lower, lies only slightly below that of GrH.

B. Electronic properties

Having briefly considered the thermodynamic stabilities of the heavy-halogen substituted graphene derivatives we will now turn to their electronic properties. We will focus our detailed analysis on the more stable fluorinated derivatives, beginning by looking at both the PBE as well as the GLLB-SC band structures. The corresponding plots are shown in Fig. 2 and allow us to make some very interesting observations:

1. PBE predicts significantly lower band gaps than GLLB-SC in all cases with BrFF being predicted to be conducting at the PBE level while a gap is present in the GLLB-SC results.

2. All structures show strong band-dispersion along the \( \Gamma \rightarrow M \) and \( \Gamma \rightarrow K \) directions while bands close to the Fermi energy \( E_F \) are nearly flat along the \( \Gamma \rightarrow M \) direction.

3. Substitution of Br by Cl leads to an increased splitting of the bands close to the Fermi energy.

Let us start by considering the first of these observations: electrons occupying conduction and valence bands close to the Fermi energy are highly localized along one spatial direction in all systems as evidenced by the low dispersion of these bands along the \( \Gamma \rightarrow M \) direction while the dispersive nature of the bands along \( \Gamma \rightarrow M' \) indicates a large degree of delocalization. This characteristic feature of the band structure results in a strong 1D localization of the occupied bands close to the Fermi energy (see also Fig. 3). This means the overlap between charge densities in different unit cells is large along one spatial direction whereas it is small to negligible along the other. The failure of PBE to correctly describe the systems band gap is therefore likely attributable to the known failures of GGA-functionals in describing localized systems of electrons. \(^5\) GLLB-SC on the other hand, through approximating the OEP-EXX
functional, better describes the important on site interactions and yields finite band gaps for all three systems shown in Fig. 2.

We now compare band gap values at the GLLB-SC and GLLB-SC + Δxc level to band gaps calculated using the HSE03 screened...
hybrid functional within the CRYSTAL14 code. Results are summarized in Table 2. As expected, GLLB-SC is able to correctly reproduce the trends seen in the HSE03 results, predicting all three systems to be semi-conducting. Upon including the derivative discontinuity, the agreement is further improved with band gaps for BrFBr and BrFCl being close to identical in the two methods. The difference is somewhat larger in the case of BrFF, though we are unsure as to what causes this discrepancy. This good agreement between results at the HSE03 and GLLB-SC + \( \Delta_X \) level combined with the demonstrated success of HSE03 as a starting point for \( G_0W_0 \) calculations makes GLLB-SC + \( \Delta_X \) seem to be an excellent starting point for \( G_0W_0 \) calculations given the low computational cost of GLLB-SC as compared to hybrid-functional calculations.

We stress though that, lacking experimental validation, it is unclear whether or not GLLB-SC + \( \Delta_X \) underestimates the macroscopic dielectric constants in our systems as has been shown for both HSE03\(^{31}\) as well as GLLB-SC + \( \Delta_X \)\(^{44}\) in a series of other materials and if so, how this affects the quality of \( G_0W_0 \) results. For this reasons we have performed both \( G_0W_0 @ GLLB-SC \) as well as \( G_0W_0 @ GLLB-SC + \Delta_X \) calculations which might serve as two limiting cases for the true quasiparticle gap. The results of these are also given in Table 2 and, unsurprisingly, show an opening of the \( G_0W_0 \) gap upon inclusion of the derivative discontinuity.

Returning now to the band structures shown in Fig. 2 it is worth considering the nature of the highly-localized states close to the Fermi energy (\( E_F \)). To do so in Fig. 3 we have shown the band structures of BrFBr and BrFCl together with charge-density plots representing the three bands close to \( E_F \) at the \( \Gamma \)-point. In BrFBr both of the closely-spaced occupied bands show strong localization on the chains of bromine atoms along the 2D structure while the unoccupied band forming the conduction band minimum (CBM) is largely delocalized over the entirety of the layer. Upon Br → Cl substitution, while the band forming the CBM is not visibly altered, the two closely-spaced, occupied bands lying close to \( E_F \) in BrFBr are split significantly. The origin of this split can again be understood from looking at the charge density plots. While the two bands in question are delocalized over the Br atoms lying on both sides of the 2D layer in BrFBr, they become localized on only one side in the case of BrFCl with the band localized on the Cl-side being pushed down in energy with respect to the Br-localized one.

| Table 2 | Direct fundamental gaps for fluorinated systems using different DFT functionals and methods. While HSE03 calculations are performed using an LCAO basis within the CRYSTAL14 code, all other calculations employ a plane-wave basis and are performed using the GPAW program |
|---------|---------------------------------------------------------------|
|         | BrFF             | BrFBr            | BrFCl             |
| HSE03   | 0.73             | 1.46             | 1.26              |
| GLLB-SC | 0.40             | 1.16             | 0.95              |
| GLLB-SC + \( \Delta_X \) | 0.52             | 1.54             | 1.25              |
| \( G_0W_0 @ GLLB-SC \) | 3.14             | 3.52             | 3.47              |
| \( G_0W_0 @ GLLB-SC + \Delta_X \) | 3.29             | 3.96             | 3.82              |

IV. Optical properties

Since we are interested in the optical properties of our systems in particular as they relate to possible applications in photovoltaics, effects due to exciton binding cannot be neglected, especially as they are expected to be of even greater importance in low-dimensional systems such as those considered here\(^{16,19} \).
as compared to 3D ones. We therefore performed BSE calculations employing both $G_0W_0@\text{GLLB-SC}$ as well as $G_0W_0@\text{GLLB-SC} + A_{\text{xc}}$ as a starting point. Fig. 4 shows the resulting spectra in the optical limit ($q \rightarrow 0$) at different levels of theory and for different directions of the incoming photons. As expected from the systems band structure shown in Fig. 2, the lowest-lying exciton is localized along the $\hat{Y}$-direction while the first peak along $\hat{X}$ lies at $\approx 2.49$ eV showing very low intensity as compared to the peak along $\hat{Y}$. Comparing the curves shown on the right-hand side of Fig. 4 we can further see that, as expected for a 2D material, electron–hole interactions play a significant role in determining the position of the first optical adsorption peaks with spectra at the RPA level being strongly blue-shifted compared to their BSE counterparts.

Another interesting observation that can be made from Table 4 is the fact that substituting one of the bromine atoms in the unit cell by chlorine and finally fluorine, i.e., moving from BrFBr to BrFCl and BrFF, significantly affects the position of the first excitation peak. While Cl → F substitution leaves the exciton binding energy (i.e., the difference between the fundamental and the optical gap) nearly unaltered at $\approx 1.8$ eV, interchanging Cl/F with Br (i.e., going from BrFCl/BrFF to BrFBr) lowers it by $\approx 0.2$ eV. This change is made all the more interesting by the fact that the change in the $G_0W_0$ gap is 0.34 eV and 0.53 eV upon Cl → F substitution using $G_0W_0@\text{GLLB-SC}$ and $G_0W_0@\text{GLLB-SC} + A_{\text{xc}}$ respectively, while the $G_0W_0@\text{GLLB-SC}/G_0W_0@\text{GLLB-SC} + A_{\text{xc}}$ gaps of BrFBr and BrFCl only differ by 0.05/0.14 eV. To understand the origin of the effect we return briefly to the discussion of the band structures shown in Fig. 3. While pure bromine systems show two almost degenerate bands at the Fermi energy, one of these bands is significantly lowered in energy upon substituting bromine by chlorine which leads to the exciton becoming localized in only one of the two bands. As this band is localized on only one side of the 2D layer in BrFCl and BrFF as compared to both sides of the layer in BrFBr, the spatial localization of the exciton increases which in turn leads to an increase in the exciton binding energy. Finally, we note that the first adsorption peak for all three systems lies close to the optimal peak position for photovoltaic applications at $\approx 1.5$ eV.\textsuperscript{56,57} In particular BrFF, which shows a first adsorption peak at $\approx 1.3–1.4$ eV (depending on the level of theory) and displays predicted stability higher than that of graphene constitutes a very promising candidate for application in future solar technology.

### V. Conclusions

Herein we have studied the thermodynamic stability and optoelectronic properties of a series of heavy-halogen substituted graphene and fluorographene derivatives, based on the work originally done by Karlický, Zbořil and Otyepka.\textsuperscript{22} Graphane-based systems show predicted stabilities lower than graphene, whilst still exceeding that of chlorographene. Fluorographene-based systems on the other hand were shown to display stabilities on par with and even exceeding that of graphene.

We studied in detail the electronic structure of the aforementioned systems, showing them to display strong 1D-localization of charge carriers with a marked electron–hole asymmetry which we hypothesize might be exploited in separating electron–hole pairs created upon photoexcitation.

Employing the GLLB-SC functional we were able to obtain band gaps which closely reproduce HSE03 results while...
keeping computational costs to approximately those of GGA calculations. Given the success of the \(G_0W_0\)@HSE03 approach in predicting the band gaps of a number of materials,\(^{51}\) we believe it to provide an excellent starting point for \(G_0W_0\) calculations, combining low computational requirements with good accuracy.

Lastly we investigated the optical spectra of the systems including electron–hole interactions on top of \(G_0W_0\) by solving the Bethe–Salpeter equation. The first optical adsorption peak for all the systems considered lies close to the optimal peak position given by the Shockley–Queisser limit, i.e. \(\approx 1.5 \text{ eV}.^{56,57}\) Especially BrFF, who's first adsorption peak lies at \(\approx 1.3–1.4 \text{ eV}\) and which shows a predicted stability higher than that of graphene constitutes a very promising candidate for application in future solar technology.

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