Modern Astrophysics is based on multi-wavelength data organized into large and heterogeneous catalogs. Hence, the need for efficient, reliable and scalable catalog cross-matching methods plays a crucial role in the era of the petabyte scale. Furthermore, multi-band data have often very different angular resolution, requiring the highest generality of cross-matching features, mainly in terms of region shape and resolution. In this work we present C$^3$ (Command-line Catalog Cross-match), a multi-platform application designed to efficiently cross-match massive catalogs. It is based on a multi-core parallel processing paradigm and conceived to be executed as a stand-alone command-line process or integrated within any generic data reduction/analysis pipeline, providing the maximum flexibility to the end-user, in terms of portability, parameter configuration, catalog formats, angular resolution, region shapes, coordinate units and cross-matching types. Using real data, extracted from public surveys, we discuss the cross-matching capabilities and computing time efficiency also through a direct comparison with some publicly available tools, chosen among the most used within the community, and representative of different interface paradigms. We verified that the C$^3$ tool has excellent capabilities to perform an efficient and reliable cross-matching between large data sets. Although the elliptical cross-match and the parametric handling of angular orientation and offset are known concepts in the astrophysical context, their availability in the presented command-line tool makes C$^3$ competitive in the context of public astronomical tools.

Key words: catalogs – methods: data analysis – surveys – techniques: miscellaneous

Online material: color figures

1. Introduction

In the last decade we entered the data-intensive era of astrophysics, where the size of data has rapidly increased, reaching in many cases dimensions overcoming the human possibility to handle them in an efficient and comprehensible way. In a very close future petabytes of data will be the standard and, to deal with such amount of information, also the data analysis techniques and facilities must quickly evolve. For example the current exploration of petabyte-scale, multi-disciplinary astronomy and Earth observation synergy, by taking the advantage from their similarities in data analytics, has issued the urgency to find and develop common strategies able to achieve solutions in the data mining algorithms, computer technologies, large scale distributed database management systems as well as parallel processing frameworks (Agrafioti et al. 2012).

Astrophysics is one of the most involved research fields facing with this data explosion, where the data volumes from the ongoing and next generation multi-band and multi-epoch surveys are expected to be so huge that the ability of the astronomers to analyze, cross-correlate and extract knowledge from such data will represent a challenge for scientists and computer engineers. To quote just a few, the ESA Euclid space mission will acquire and process about 100 GB day$^{-1}$ over at least 6 years, collecting a minimum amount of about 200 TB of data (Laureijis et al. 2014); Pan-STARRS (Kaiser 2004) is expected to produce more than 100 TB of data; the GAIA space mission will build a 3D map of the Milky Way galaxy, by collecting about one petabyte of data in five years (Douglas et al. 2007); the Large Synoptic Survey Telescope (Ivezic 2009) will provide about 20 TB/night of imaging data for ten years and petabytes/year of radio data products. Many other planned instruments and already operative surveys will reach a huge scale during their operational lifetime, such as KiDS (Kilo-Degree Survey; de Jong et al. 2015), DES (Dark Energy Survey, Annis 2013), Herschel-ATLAS (Valiante 2015; Varga-Verebelyi et al. 2016), Hi-GAL (Molinari et al. 2016), SKA (Braun 2015) and E-ELT (Martins et al. 2014).

The growth and heterogeneity of data availability induce challenges on cross-correlation algorithms and methods. Most of the interesting research fields are in fact based on the capability and efficiency to cross-correlate information among different surveys. This poses the consequent problem of
transferring large volumes of data from/to data centers, *de facto* making almost inoperable any cross-reference analysis, unless to change the perspective, by moving software to the data (Cavuoti et al. 2012).

Furthermore, observed data coming from different surveys, even if referred to a same sky region, are often archived and reduced by different systems and technologies. This implies that the resulting catalogs, containing billions of sources, may have very different formats, naming schemas, data structures and resolution, making the data analysis to be a not trivial challenge. Some past attempts have been explored to propose standard solutions to introduce the uniformity of astronomical data quantities description, such as in the case of the Uniform Content Descriptors of the Virtual Observatory (IVOA Recommendation 2005).

One of the most common techniques used in astrophysics and fundamental prerequisite for combining multi-band data, particularly sensible to the growing of the data sets dimensions, is the cross-match among heterogeneous catalogs, which consists in identifying and comparing sources belonging to different observations, performed at different wavelengths or under different conditions. This makes cross-match one of the core steps of any standard modern pipeline of data reduction/analysis and one of the central components of the Virtual Observatory (Malkov et al. 2012).

The massive multi-band and multi-epoch information, foreseen to be available from the on-going and future surveys, will require efficient techniques and software solutions to be directly integrated into the reduction pipelines, making possible to cross-correlate in real time a large variety of parameters for billions of sky objects. Important astrophysical questions, such as the evolution of star forming regions, the galaxy formation, the distribution of dark matter and the nature of dark energy, could be addressed by monitoring and correlating fluxes at different wavelengths, morphological and structural parameters at different epochs, as well as by opportune determining their cosmological distances and by identifying and classifying peculiar objects. In such context, an efficient, reliable and flexible cross-matching mechanism plays a crucial role. In this work we present $C^3$ (*Command-line Catalog Cross-match*), a tool to perform efficient catalog cross-matching, based on the multi-thread paradigm, which can be easily integrated into an automatic data analysis pipeline and scientifically validated on some real case examples taken from public astronomical data archives. Furthermore, one of major features of this tool is the possibility to choose shape, orientation and size of the cross-matching area, respectively, between elliptical and rectangular, clockwise and counterclockwise, fixed and parametric. This makes the $C^3$ tool easily tailored on the specific user needs.

The paper is structured as follows: after a preliminary introduction, in Section 2 we perform a summary of main available techniques; in Section 3, the design and architecture of the $C^3$ tool is described; in Sections 4 and 5, the procedure to correctly use $C^3$ is illustrated with particular reference to the optimization of its parameters; some tests performed in order to evaluate $C^3$ performance are shown in Section 6; finally, conclusions and future improvements are drawn in Section 7.

2. Cross-matching Techniques

Cross-match can be used to find detections surrounding a given source or to perform one-to-one matches in order to combine physical properties or to study the temporal evolution of a set of sources.

The primary criterion for cross-matching is the approximate coincidence of celestial coordinates (positional cross-match). There are also other kinds of approach, which make use of the positional mechanism supplemented by statistical analysis used to select best candidates, like the bayesian statistics (Budavári & Szalay 2008). In the positional cross-match, the only attributes under consideration are the spatial information. This kind of match is of fundamental importance in astronomy, due to the fact that the same object may have different coordinates in various catalogs, for several reasons: measurement errors, instrument sensitivities, calibration, physical constraints, etc.

In principle, at the base of any kind of catalog cross-match, each source of a first catalog should be compared with all counterparts contained in a second catalog. This procedure, if performed in the naive way, is extremely time consuming, due to the huge amount of sources. Therefore different solutions to this problem have been proposed, taking advantage of the progress in computer science in the field of multi-processing and high performing techniques of sky partitioning. Two different strategies to implement cross-matching tools basically exist: web and stand-alone applications.

Web applications, like OpenSkyQuery (Nieto-Santisteban et al. 2006), or CDS-Xmatch (Pineau et al. 2011), offer a portal to the astronomers, allowing to cross-match large astronomical data sets, either mirrored from worldwide distributed data centers or directly uploadable from the user local machine, through an intuitive user interface. The end-user has not the need to know how the data are treated, delegating all the computational choices to the backend software, in particular for what is concerning the data handling for the concurrent parallelization mechanism. Other web applications, like ARCHES (Motch 2015), provide dedicated script languages which, on one hand, allow to perform complex cross-correlations while controlling the full process but, on the other hand, make experiment settings quite hard for an astronomer. Basically, main limitation of a web-based approach is the impossibility to directly use the cross-matching tool in an automatic pipeline of data reduction/analysis. In other words,
with such a tool the user cannot design and implement a complete automatic procedure to deal with data. Moreover, the management of concurrent jobs and the number of simultaneous users can limit the scalability of the tool. For example, a registered user of CDS-Xmatch has only 500 MB disk space available to store his own data (reduced to 100 MB for unregistered users) and all jobs are aborted if the computation time exceeds 100 minutes (Boch et al. 2014). Finally, the choice of parameters and/or functional cases is often limited in order to guarantee a basic use by the end-users through short web forms (for instance, in CDS-Xmatch only equatorial coordinate system is allowed).

Stand-alone applications are generally command-line tools that can be run on the end-user machine as well as on a distributed computing environment. A stand-alone application generally makes use of APIs (Application Programming Interfaces), a set of routines, protocols and tools integrated in the code. There are several examples of available APIs, implementing astronomical facilities, such as STIL (Taylor 2006), and astroML (Vanderplas et al. 2012), that can be integrated by an astronomer within its own source code. However, this requires the astronomer to be aware of strong programming skills. Moreover, when the tools are executed on any local machine, it is evident that such applications may be not able to exploit the power of distributed computing, limiting the performance and requiring the storage of the catalogs on the hosting machine, besides the problem of platform dependency.

On the contrary, a ready-to-use stand-alone tool, already conceived and implemented to embed the use of APIs in the best way, will result an off-the-shelf product that the end-user has only to run. A local command-line tool can be put in a pipeline through easy system calls, thus giving the possibility to the end-user to create a custom data analysis/reduction procedure without writing or modifying any source code. Moreover, being an all-in-one package, i.e., including all the required libraries and routines, a stand-alone application can be easily used in a distributed computing environment, by simply uploading the code and the data on the working nodes of the available computing infrastructure.

One of the most used stand-alone tools is STILTS (STIL Tool Set, Taylor 2006). It is not only a cross-matching software, but also a set of command-line tools based on the STIL libraries, to process tabular data. It is written in pure Java (almost platform independent) and contains a large number of facilities for table analysis, so being a very powerful instrument for the astronomers. On one hand, the general-purpose nature of STILTS has the drawback to make hard the syntax for the composition of the command line; on the other hand, it does not support the full range of cross-matching options provided by C^3. In order to provide a more user-friendly tool to the astronomers, it is also available its graphical counterpart, Tool for OPerations on Catalogs And Tables (TOPCAT, Taylor 2005), an interactive graphical viewer and editor for tabular data, based on STIL APIs and implementing the STILTS functionalities, but with all the intrinsic limitations of the graphical tools, very similar to the web applications in terms of use.

Regardless the approach to cross-match the astronomical sources, the main problem is to minimize the computational time exploding with the increasing of the matching catalog size. In principle, the code can be designed according to multi-process and/or multi-thread paradigm, so exploiting the hosting machine features. For instance, Lee & Budavári (2013) evaluated to use a multi-GPU environment, designing and developing their own Xmatch tool, (Budavári & Lee 2013). Other studies are focused to efficiently cross-match large astronomical catalogs on clusters consisting of heterogeneous processors including both multi-core CPUs and GPUs, (Jia et al. 2015; Jia & Luo 2016). Furthermore, it is possible to reduce the number of sources to be compared among catalogs, by opportunistically partitioning the sky through indexing functions and determining only a specific area to be analyzed for each source. CDS-Xmatch and the tool described in Zhao et al. (2009, p. 604) use Hierarchical Equal Area isoLatitude Pixelisation (HEALPix, Gorski et al. 2005), to create such sky partition. Du et al. (2014), instead, proposed a combined method to speed up the cross-match by using HTM (Hierarchical Triangle Mesh, Kunszt et al. 2001), in combination with HEALPix and by submitting the analysis to a pool of threads.

HEALPix is a genuinely curvilinear partition of the sphere into exactly equal area quadrilaterals of varying shape (see Figure 3 in Gorski et al. 2005). The base-resolution comprises twelve pixels in three rings around the poles and equator. Each pixel is partitioned into four smaller quadrilaterals in the next level. The strategy of HTM is the same of HEALPix. The difference between the two spatial-indexing functions is that HTM partitioning is based on triangles, starting with eight triangles, 4 on the Northern and 4 on the Southern hemisphere, each one partitioned into four smaller triangles at the next level (see also Figure 2 in Du et al. 2014). By using one or both functions combined together, it is possible to reduce the number of comparisons among objects to ones lying in adjacent areas.

Finally, OpenSkyQuery uses the Zones indexing algorithm to efficiently support spatial queries on the sphere, (Gray et al. 2006).

The basic idea behind the Zones method is to map the sphere into stripes of a certain height h, called zones. Each object with coordinates (ra, dec) is assigned to a zone by using the
formula:

\[
\text{zoneID} = \text{dec} + 90.0/h
\]  

A traditional B-tree index is then used to store objects within a zone, ordered by zoneID and right ascension. In this way, the spatial cross-matching can be performed by using bounding boxes (B-tree ranges) dynamically computed, thus reducing the number of comparisons (Figure 1 in Nieto-Santisteban et al. 2006). Finally, an additional and expensive test allows to discard false positives.

All the cross-matching algorithms based on a sky partitioning have to deal with the so-called block-edge problem, illustrated in Figure 1: the objects \(X\) and \(X'\) in different catalogs correspond to the same object but, falling in different pieces of the sky partition, the cross-matching algorithm is not able to identify the match. To solve this issue, it is necessary to add further steps to the pipeline, inevitably increasing the computational time. For example, the Zhao’s tool (Zhao et al. 2009), expands a Healpix block with an opportunely dimensioned border; instead, the algorithm described by Du et al. (2014), combining Healpix and HTM virtual indexing function shapes, is able to reduce the block-edge problem, because the lost objects in a partition may be different from one to another.

3. \(C^3\) Design and Architecture

\(C^3\) is a command-line open-source Python script, designed and developed to perform a wide range of cross-matching types among astrophysical catalogs. The tool is able to be easily executed as a stand-alone process or integrated within any generic data reduction/analysis pipeline. Based on a specialized sky partitioning function, its high-performance capability is ensured by making use of the multi-core parallel processing paradigm. It is designed to deal with massive catalogs in different formats, with the maximum flexibility given to the end-user, in terms of catalog parameters, file formats, coordinates and cross-matching functions.

In \(C^3\) different functional cases and matching criteria have been implemented, as well as the most used join function types. It also works with the most common catalog formats, with or without header: Flexible Image Transport System (FITS, version tabular), American Standard Code for Information Interchange (ASCII, ordinary text, i.e., space separated values), Comma Separated Values (CSV), Virtual Observatory Table (VOTable, XML based) and with two kinds of coordinate system, equatorial and galactic, by using STILTS in combination with some standard Python libraries, namely NumPy\(^8\) (Van Der Walt et al. 2011), and PyFITS\(^9\).

Despite the general purpose of the tool, reflected in a variety of possible functional cases, \(C^3\) is easy to use and to configure through few lines in a single configuration file. Main features of \(C^3\) are the following:

1. **Command line**: \(C^3\) is a command-line tool. It can be used as stand-alone process or integrated within more complex pipelines;
2. **Python compatibility**: compatible with Python 2.7.x and 3.4.x (up to the latest version currently available, 3.5);
3. **Multi-platform**: \(C^3\) has been tested on Ubuntu Linux 14.04, Windows 7 and 10, Mac OS and Fedora;
4. **Multi-process**: the cross-matching process has been developed to run by using a multi-core parallel processing paradigm;
5. **User-friendliness**: the tool is very simple to configure and to use; it requires only a configuration file, described in Section 4.

The internal cross-matching mechanism is based on the sky partitioning into cells, whose dimensions are determined by the parameters used to match the catalogs. The sky partitioning procedure is described in Section 3.3.1. The Figure 2 shows the most relevant features of the \(C^3\) processing flow and the user parameters available at each stage.

3.1. Functional Cases

As mentioned before, the user can run \(C^3\) to match two input catalogs by choosing among three different functional cases:

1. **Sky**: the cross-match is done within sky areas (elliptical or rectangular) defined by the celestial coordinates taken from catalog parameters;
2. **Exact Value**: two objects are matched if they have the same value for a pair of columns (one for each catalog) defined by the user;

---

8. [http://www.numpy.org/](http://www.numpy.org/)

9. PyFITS is a product of the Space Telescope Science Institute, which is operated by AURA for NASA. [http://www.stsci.edu/institute/software_hardware/pyfits](http://www.stsci.edu/institute/software_hardware/pyfits).
3. **Row-by-Row**: match done on a same row-ID of the two catalogs. The only requirement here is that the input catalogs must have the same number of records.

The positional cross-match strategy of the $C^3$ method is based on the same concept of the Q-FULLTREE approach, an our tool introduced in Becciani et al. (2015) and Sciacca et al. (2016): for each object of the first input catalog, it is possible to define an elliptical, circular or rectangular region centered on its coordinates, whose dimensions are limited by a fixed value or defined by specific catalog parameters. For instance, the two Full Width at Half Maximum (FWHM) values in the catalog can define the two semi-axes of an ellipse or the couple width and height of a rectangular region. It is also possible to have a circular region, by defining an elliptical area having equal dimensions. Once defined the region of interest, the next step is to search for sources of the second catalog within such region, by comparing their distance from the central object and the limits of the area (for instance, in the elliptical cross-match the limits are defined by the analytical equation of the ellipse).

In the *Sky* functional case, the user can set additional parameters in order to characterize the matching region and the properties of the input catalogs. In particular, the user may define

1. the shape (elliptical or rectangular) of the matching area, i.e., the region, centered on one of the matching sources, in which to search the objects of the second catalog;
2. the dimensions of the searching area. They can be defined by fixed values (in arcseconds) or by parametric values coming from the catalog. Moreover, the region can be rotated by a position angle (defined as fixed value or by a specific column present in the catalog);
3. the coordinate system for each catalog (galactic, icrs, fk4, fk5) and its units (degrees, radians, sexagesimal), as well as the columns containing information about position and designation of the sources.

An example of graphical representation of an elliptical cross-match is shown in Figure 3.

In the *Exact Value* case, the user has to define only which columns (one for each input catalog) have to be matched, while
in the most simple Row-by-Row case no particular configuration is needed.

### 3.2. Match Selection And join Types

$C^3$ produces a file containing the results of the cross-match, consisting into a series of rows, corresponding to the matching objects. In the case of Exact value and Sky options, the user can define the conditions to be satisfied by the matched rows to be stored in the output. First, it is possible to retrieve, for each source, all the matches or only the best pairs (in the sense of closest objects, according to the match selection criterion); then, the user can choose different join possibilities (in Figure 4 the graphical representation of available joins is shown):

- **1 and 2**: only rows having an entry in both input catalogs, (Figure 4(a));
- **1 or 2**: all rows, matched and unmatched, from both input catalogs, (Figure 4(b));
- **All from 1 (All from 2)**: all matched rows from catalog 1 (or 2), together with the unmatched rows from catalog 1 (or 2), (Figures 4(c)–(d));
- **1 not 2 (2 not 1)**: all the rows of catalog 1 (or 2) without matches in the catalog 2 (or 1), (Figures 4(e)–(f));
- **1 xor 2**: the “exclusive or” of the match—i.e., only rows from the catalog 1 not having matches in the catalog 2 and viceversa, (Figure 4(g)).

### 3.3. Execution Phases

Any experiment with the $C^3$ tool is based on two main phases (see Figure 2):

1. **Pre-matching**: this is the first task performed by $C^3$ during execution. The tool manipulates input catalogs to extract the required information and prepare them to the further analysis;
2. **Matching**: after data preparation, $C^3$ performs the matching according to the criteria defined in the configuration file.

Finally, the results are stored in a file, according to the match criterion described in Section 3.2, and all the temporary data are automatically deleted.

#### 3.3.1. Pre-matching

This is the preliminary task performed by $C^3$ execution. During the pre-matching phase, $C^3$ performs a series of preparatory manipulations on input data. First of all, a validity check of the configuration parameters and input files. Then it is necessary to split the data sets in order to parallelize the matching phase and improve the performance. In the Exact Value functional case only the first input catalog will be split, while in the Sky case both data sets will be partitioned in subsets. In the latter case, $C^3$ makes always use of galactic...
coordinates expressed in degrees, thus converting them accordingly if expressed in different format.

When required, the two catalogs are split in the following way: in the first catalog all the entries are divided in groups, whose number depends on the multi-processing settings (see Section 4), since each process is assigned to one group; in the second catalog the sky region defined by the data set is divided into square cells, by assigning a cell to each entry, according to its coordinates (Figure 5).

We used the Python multiprocess module to overcome the GIL problem, by devoting particular care to the granularity of data to be handled in parallel. This implies that the concurrent processes do not need to share resources, since each process receives different files in input (group of object of the first catalog and cells) and produces its own output. Finally the results are merged to produce the final output.

The partitioning procedure on the second catalog is based on the dimensions of the matching areas: the size of the unit cell is defined by the maximum dimension that the elliptical matching regions can assume. If the “Size type” is “parametric,” then the maximum value of the columns indicated in the configuration is used as cell size; in the case of “fixed” values, the size of the cell will be the maximum of the two values defined in the configuration (Figure 5(a)). In order to optimize the performance, the size of the unit cell cannot be less than a threshold value, namely the minimum partition cell size, which the user has to set through the configuration file. The threshold on the cell size is required in order to avoid the risk to divide the sky in too many small areas (each one corresponding to a file stored on the disk), which could slow down the cross-matching phase performance. In Section 5 we illustrated a method to optimize such parameter as well as the number of processes to use, according to the hosting machine properties.

Once the partitioning is defined, each object of the second catalog is assigned to one cell, according to its coordinates. Having defined the cells, the boundaries of an elliptical region associated to an object can fall at maximum in the eight cells surrounding the one including the object, as shown in Figure 5(b). This prevents the block-edge problem previously introduced.

3.3.2. Matching

Once the data have been properly re-arranged, the cross-match analysis can start. In the Row-by-Row case, each row of the first catalog is simply merged with the corresponding row of the second data set through a serial procedure. In the other functional cases, the cross-matching procedure has been designed and implemented to run by using parallel processing, i.e., by assigning to each parallel process one group generated in the previous phase. In the Exact Value case, each object of the group is compared with all the records of the second catalog and matched according to the conditions defined in the configuration file.

In the Sky functional case, the matching procedure is slightly more complex. As described in Section 3.1, the cross-match at the basis of the $C^3$ method is based on the relative position of two objects: for each object of the first input catalog, $C^3$ defines the elliptical/rectangular region centered on its coordinates and dimensions. Therefore a source of the second catalog is matched if it falls within such region.

In practice, as explained in the pre-matching phase, having identified a specific cell for each object of a group, this information is used to define the minimum region around the object used for the matching analysis. The described choice to set the dimensions of the cells ensures that, if a source matches with the object, it must lie in the nine cells surrounding the object (also known as Moore’s neighborhood, Gray (2003), see also Figure 5(b)). Therefore it is sufficient to cross-match an object of a group only with the sources falling in nine cells.

In the Sky functional case, $C^3$ performs a cross-matching of objects lying within an elliptical, circular or rectangular area, centered on the sources of the first input catalog. The matching area is characterized by 6 configuration parameters defining its shape, dimensions and orientation. In Figure 6 is depicted a graphical representation of two matching areas (elliptical and rectangular) with the indication of its parameters.

In particular, to define the orientation of the matching area, $C^3$ requires two further parameters besides the offset and the value of the position angle, representing its orientation. The position angle, indeed, is referred, by default, to the greatest
axis of the matching area with a clockwise orientation. The two additional parameters give the possibility to indicate, respectively, the correct orientation (clockwise/counterclockwise) and a shift angle (in degrees).

Finally, the results of the cross-matching are stored in a file, containing the concatenation of all the columns of the input catalogs referred to the matched rows. In the Sky functional case the column reporting the separation distance between the two matching objects is also included.

4. Configuration

The tool C³ is interfaced with the user through a single configuration file, to be properly edited just before the execution of any experiment. If the catalogs do not contain the source’s Designation/ID information, C³ will automatically assign an incremental row-ID to each entry as object designation.

For the Sky functional case, assuming that both input catalogs contain the columns reporting the object coordinates, C³ is able to work with galactic and equatorial (icrs, fk4, fk5) coordinate systems, expressed in the following units: degrees, radians or sexagesimal.

If the user wants to use catalog information to define the matching region (for instance, the FWHMs or a radius defined by the instrumental resolution), obviously the first input catalog must contain such data. The position angle value/column is, on the contrary, an optional information (default is 0°, clockwise).

C³ is conceived for a community as wide as possible, hence it has been designed in order to satisfy the requirement of user-friendliness. Therefore, the configuration phase is limited to the editing of a setup file, containing all the information required to run C³. This file is structured in sections, identified by square brackets: the first two are required, while the others depend on the particular use case. In particular, the user has to provide the following information:

1. the input files and their format (FITS, ASCII, CSV or VOTable);
2. the name and paths of the temporary, log and output files;
3. the match criterion, corresponding to one of the functional cases (Sky, Exact Value, Row-by-Row).

C³ gives also the possibility to set the number of processes running in parallel, through an optional parameter which has as default the number of cores of the working machine (minus one left available for system auxiliary tasks).

4.1. Sky Functional Case

The configuration for the Sky functional case foresees the setup of specific parameters of the configuration file: those required to define the shape and dimensions of the matching area, the properties of the input catalogs already mentioned in Section 3.1, coordinate system, units as well as the column indexes for source coordinates and designation. In addition, a parameter characterizing the sky partitioning has to be set (see Section 3.3.1 for further information).

The parameters useful to characterize the matching area are the following:

Area shape: it can be elliptical or rectangular (circular is a special elliptical case);
Size type: the valid entries are fixed or parametric. In the first case, a fixed value will be used to determine the matching area; in the second, the dimensions and inclination of the matching area will be calculated by using catalog parameters;
First and second dimensions of matching area: the axes of the ellipse or width and height of the rectangular area. In case of fixed “Size type,” they are decimal values (in arcsec), otherwise, they represent the index (integer) or name

---

10 C³ can also automatically generate a dummy configuration file that could be used as template.
(string) of the columns containing the information to be used;

**Parametric factor:** it is required and used only in the case of parametric “Size type.” It is a decimal number factor to be multiplied by the values used as dimensions, in order to increase or decrease the matching region, as well as useful to convert their format;

**Pa column/value:** it is the position angle value (in the “fixed” case, expressed in degrees) or the name/ID of the column containing the position angle information (in the “parametric” case);

**Pa settings:** the position angle, which in \( C^3 \) is referred, by default, to the main axis of the matching area (greatest) with a clockwise orientation. The two parameters defined here give the possibility to indicate the correct orientation (clockwise/counterclockwise) and a shift angle (in degrees).

The user also has to specify which rows must be included in the output file, by setting the two parameters indicating the match selection and the join type, as described in Section 3.2.

### 4.2. Exact Value Functional Case

For the **Exact value** functional case it is required to set the name or id of the columns used for the match for both input files. The user also has to specify which rows must be included in the output file, by setting the two parameters indicating the match selection and the join type, as described in Section 3.2.

### 4.3. Row-by-Row Functional Case

For the **Row-by-Row** functional case, no other settings are required. The only constrain is that both catalogs must have the same number of entries.

### 5. Computational Optimization Procedure

As reflected from the description of \( C^3 \), the choice of the best values for its internal parameters (in particular the number of parallel processes and the minimum cell size, introduced in Section 3.3.1), is crucial to obtain the best computational efficiency. This section is dedicated to show the importance of this choice, directly depending on the features of the hosting machine. In the following tests we used a computer equipped with an Intel(R) Core(TM) i5-4460, with one 3.20 GHz, 4-core CPU, 32 GB of RAM and hosting Ubuntu Linux 14.04 as operative system (OS) on a standard Hard Disk Drive. We proceeded by performing two different kinds of tests:

1. a series of tests with a fixed value for the minimum cell size (100°) and different values of the number of parallel processes;

2. a second series by using the best value of number of parallel processes found at previous step and different values for the minimum cell size.

The configuration parameters used in this set of tests are reported in Table 1. The input data sets are two identical catalogs (CSV format) consisting of 100,000 objects extracted from the UKIDSS GPS public data (Lucas et al. 2008), in the range of galactic coordinates \( l \in [50, 60], b \in [-1, 1] \). Each record is composed by 125 columns. The choice to cross-match a catalog with itself represent the worst case in terms of cross-matching computational time, since each object matches at least with itself.

| Parameter               | Value |
|-------------------------|-------|
| Area Shape              | Ellipse|
| Size Type               | Fixed |
| First dimension (Major axis) | 5°   |
| Second dimension (Secondary axis) | 5° |
| Position Angle settings | 0°    |
| Coordinate System       | Galactic (deg) |
| Match Selection         | best  |
| Join type               | 1 and 2 |

**Note.** The choice of same dimensions for the ellipse axes was due to perform a fair comparison with STILTS and CDS-Xmatch, which allow only circular cross-matching.
In more general terms, the described example demonstrates that, in order to obtain the best computational performance, the configuration requires a series of heuristics to reach the best compromise between the granularity of the parallel processing and the scheduling management of the OS. As rule of thumb, the best results can be obtained by choosing the number of parallel processes limited between 10 and 100 times the number of cores of the hosting machine.

For what concerns the minimum cell size, in the previous example we considered 20 square degrees, with 100,000 objects, thus a density of ∼1 object in 2600 square arcsec

Since the best results have been obtained with a cell size of 100", we obtained ∼7 objects per cell. By extrapolating from our tests, the best cell size, conditioning the sky partitioning resolution, should be chosen between 2 and 10 sources per cell. Of course, this heuristic range depends on the specific density of the involved fields.

6. Testing on Astrophysical Data

In order to validate the results of C³ and evaluate its performance in terms of cross-matching reliability and computational time efficiency, we performed several tests on real data. In particular, two kinds of tests have been executed, both using the most complex functional case Sky. The first set of tests (Section 6.1), has been performed to validate the C³ results in terms of matching capability, through a comparison with other available cross-matching tools, for instance, STILTS and CDS-Xmatch. The second set of tests (Section 6.2), has been used to evaluate the computational time efficiency, by varying the dimensions of the input data sets (both in terms of rows and columns), again through a comparison with the other tools.
6.1. Cross-matching Validation Tests

In order to assess the reliability of the cross-matches produced by C³, we performed an intensive test campaign. In this section we report the most significative examples which well represent the behavior of the tool. This set of tests has been performed by applying our tool on two data sets with variable number of objects and by comparing the results with those obtained by other applications representative of different paradigms: stand-alone command-line (STILTS, release 3.0–7), GUI (TOPCAT, release 4.2.3) and web application (CDS-XMatch).¹¹

The first input catalog has been extracted by the UKIDSS GPS data in the range of galactic coordinates $l \in [40, 50], b \in [-1, 1]$, while the second input catalog has been extracted by the GLIMPSE Spitzer Data, (Benjamin et al. 2003 and Churchwell et al. 2009), in the same range of coordinates. From each catalog, different subsets with variable number of objects have been extracted. In particular, data sets with, respectively, 1000, 10,000, 100,000, 1,000,000 and 10,000,000 objects have been created from the first catalog, while, from second catalog, data sets with 1000, 10,000, 100,000 and 1,000,000 rows have been extracted. Then, each subset of first catalog has been cross-matched with all the subsets of the second catalog. For uniformity of comparison, due to the limitations imposed by CDS-Xmatch in terms of available disk space, it has been necessary to limit to only 3 the number of columns for all the subsets involved in the tests performed to compare C³ and CDS-Xmatch (for instance, ID and galactic coordinates). For the same reason, the data set with $10^7$ rows has not been used in the comparison between C³ and CDS-Xmatch.

The common internal configuration used in these tests is shown in Table 1, except for the “Match Selection” parameter. There was, in fact, the necessity to set it to all for uniformity of comparison with the CDS-Xmatch tool (which makes available only this option). Then the best type has been used to compare C³ with STILTS and TOPCAT. Furthermore, in all the tests, the number of parallel processes was set to 256 and the minimum cell size to 100”, corresponding to the best conditions found in the optimization process of C³ (see Section 5). Finally, we chose same dimensions of the ellipse axes in order to be aligned with other tools, which allow only circular cross-matching areas.

Concerning the comparison among C³ and the three mentioned tools, in the cases of both all and best types of matching selection, all tools provided exactly the same number of matches in the whole set of tests, thus confirming the reliability of C³ with respect to other tools (Table 4).¹²

| ID   | $N_{input1}$ | $N_{input2}$ | C³, CDS-XMatch, STILTS/TOPCAT (all) | C³, STILTS/TOPCAT (best) |
|------|--------------|--------------|-------------------------------------|--------------------------|
| T1   | 1000         | 1000         | 0                                   | 0                        |
| T2   | 1000         | 10,000       | 1                                   | 1                        |
| T3   | 1000         | 100,000      | 5                                   | 5                        |
| T4   | 10,000       | 1,000,000    | 116                                 | 116                      |
| T5   | 10,000       | 1000         | 0                                   | 0                        |
| T6   | 10,000       | 10,000       | 14                                  | 14                       |
| T7   | 10,000       | 100,000      | 116                                 | 116                      |
| T8   | 10,000       | 1,000,000    | 1260                                | 1248                     |
| T9   | 100,000      | 1000         | 12                                  | 12                       |
| T10  | 100,000      | 10,000       | 136                                 | 136                      |
| T11  | 100,000      | 100,000      | 1212                                | 1211                     |
| T12  | 100,000      | 1,000,000    | 12,711                              | 12,758                   |
| T13  | 1,000,000    | 1000         | 141                                 | 137                      |
| T14  | 1,000,000    | 10,000       | 1295                                | 1267                     |
| T15  | 1,000,000    | 100,000      | 12,701                              | 12,416                   |
| T16  | 1,000,000    | 1,000,000    | 126,965                             | 123,261                  |
| T17  | 10,000,000   | 1000         | 191                                 | 169                      |
| T18  | 10,000,000   | 10,000       | 1995                                | 1755                     |
| T19  | 10,000,000   | 100,000      | 19,717                              | 17,235                   |
| T20  | 10,000,000   | 1,000,000    | 196,310                             | 171,775                  |

Note. Column 4 reports the number of matches of the three tools in the case of all matching selection criterion (tests T17–T20 have not been performed for CDS-Xmatch), while column 5 reports the matches found using the best criterion. In both cases all tools provided exactly the same number of matches in the whole set of tests.

6.2. Performance Tests

In terms of computational efficiency, C³ has been evaluated by comparing the computational time of its cross-matching phase with the other tools. The pre-matching and output creation steps have been excluded from the comparison, because strongly dependent on the host computing infrastructure. The other configuration parameters have been left unchanged (Table 1). The complete setup for the described experiments is reported in the Appendix.

In Figure 7 we show the computational time of the cross-matching phase for C³ and STILTS, as function of the incremental number of rows (objects) in the first catalog, and by varying the size of the second catalog in four cases, spanning from 1000 to 1,000,000 rows. In all diagrams, it appears evident the difference between the two tools, becoming particularly relevant with increasing amounts of data.

In the second set of tests performed on C³ and STILTS, the computational time of the cross-matching phase has been evaluated as function of the incremental number of columns of the first catalog (from the minimum required 3 up to 125, the maximum number of columns of catalog 1), and by fixing the number of columns of the second catalog in five cases,
respectively, 3, 20, 40, 60 and 84, which is the maximum number of columns for catalog 2. In terms of number of rows, in all cases both catalogs were fixed to 1,000,000 of entries. In Figure 8 the results only for 3 and 84 columns of catalog 2 are reported, showing that $C^3$ is almost invariant to the increasing of columns, becoming indeed faster than STILTS from a certain amount of columns. Such trend is confirmed in all the other tests with different number of columns of the second catalog. This behavior appears particularly suitable in the case of massive catalogs. Finally, in the case of two FITS input files instead of CSV files, STILTS computational time as function of the number of columns is constant and slightly faster than $C^3$.

In the last series of tests, we compared the computational efficiency of the cross-matching phase between $C^3$ and CDS-Xmatch. In this case, due to the limitation of the catalog size imposed by CDS-Xmatch, the tests have been performed by...
7. Conclusions and Future Developments

In this paper we have introduced $C^3$, a new scalable tool to cross-match astronomical data sets. It is a multi-platform command-line Python script, designed to provide the maximum flexibility to the end users in terms of choice about catalog properties (I/O formats and coordinates systems), shape and size of matching area and cross-matching type. Nevertheless, it is easy to configure, by compiling a single configuration file, and to execute as a stand-alone process or integrated within any generic data reduction/analysis pipeline.

In order to ensure the high-performance capability, the tool design has been based on the multi-core parallel processing paradigm and on a basic sky partitioning function to reduce the number of matches to check, thus decreasing the global computational time. Moreover, in order to reach the best performance, the user can tune on the specific needs the shape and orientation of the matching region, as well as tailor the tool configuration to the features of the hosting machine, by properly setting the number of concurrent processes and the resolution of sky partitioning. Although the elliptical cross-match and the parametric handling of angular orientation and offset are known concepts in the astrophysical context, their availability in the presented command-line tool makes $C^3$ competitive in the context of public astronomical tools.

A test campaign, done on real public data, has been performed to scientifically validate the $C^3$ tool, showing a perfect agreement with other publicly available tools. The computing time efficiency has been also measured by comparing our tool with other applications, representative of different paradigms, from stand-alone command-line (STILTS) and graphical user interface (TOPCAT) to web applications (CDS-Xmatch). Such tests revealed the full comparable performance, in particular when input catalogs increase their size and dimensions.

For the next release of the tool, the work will be mainly focused on the optimization of the pre-matching and output creation phases, by applying the parallel processing paradigm in a more intensive way. Moreover, we are evaluating the possibility to improve the sky partitioning efficiency by optimizing the calculation of the minimum cell size, suitable also to avoid the block-edge problem.

The $C^3$ tool (Riccio et al. 2016) and the user guide are available at the page http://dame.dsf.unina.it/c3.html.

The authors would like to thank the anonymous referee for extremely valuable comments and suggestions. M.B. and S.C. acknowledge financial contribution from the agreement ASI/INAF I/023/12/1. M.B., A.M., and G.R. acknowledge financial contribution from the 7th European Framework Programme for Research Grant FP7-SPACE-2013-1, ViaLactea—The Milky Way as a Star Formation Engine. M.B. and A.M. acknowledge the PRIN-INAF 2014 Glittering kaleidoscopes in the sky: the multifaceted nature and role of Galaxy Clusters.
Appendix

Configuration File Example

This appendix reports the configuration file as used in the example described in Section 6.2. The text preceded by the semicolon is a comment.

[I/O Files]
Input catalogues 1: ./input/ukidss.csv
Format catalogues 1: csv ; csv, fits, votable or ascii
Input catalogues 2: ./input/glimpse.csv
Format catalogues 2: csv ; csv, fits, votable or ascii

[Match Criteria]
algorithm: sky ; sky, exact value, row-by-row

[Sky parameters]

---

Figure 9. Computational time of cross-matching phase as function of the number of rows of the first input catalog for C$^3$ (black) and CDS-Xmatch (red or gray) for four different dimensions of the second catalog: (a) 1000 rows, (b) 10,000 rows, (c) 100,000 rows, (d) 1,000,000 rows.

(A color version of this figure is available in the online journal.)
area shape: ellipse ; ellipse or rectangle
size type: fixed ; parametric or fixed
matching area first dimension: 5 arcsec for fixed type-
column name/number for parametric type
matching area second dimension: 5 arcsec for fixed type-
column name/number for parametric type
parametric factor: 1 ; multiplicative factor for dimen-
sion columns—required for parametric type
pa column/value: 0 ; degrees for fixed type—column name/
number for parametric type
pa settings: clock, 0 ; orientation (clock, counter),
shift (degrees) - empty or default = clock, 0
Catalogues 2 minimum partition cell size: 100 ; arcsec
[Catalogues 1 Properties]
coordinate system: galactic ; galactic, icrs, fk4, fk5
coordinate units: deg ; degrees (or deg), radians (or
rad), sexagesimal (or sex)
glon/ra column: L ; column number or name—required for sky
algorithm
glat/dec column: B ; column number or name—required for sky
algorithm
designation column: SOURCE ID ; column number or name—1
for none
[Catalogues 2 Properties]
coordinate system: galactic ; galactic, icrs, fk4, fk5
coordinate units: deg ; degrees (or deg), radians (or
rad), sexagesimal (or sex)
glon/ra column: L ; column number or name—required for sky
algorithm
glat/dec column: B ; column number or name—required for sky
algorithm
designation column: designation ; column number or name,
-1 for none
[Threads Properties]
thread limit: 256 ; maximum number of simultaneous threads
(it depends on your machine)
[Output Rows]
Match selection: all ; all or best
Join type: 1 and 2 ; 1 and 2, 1 or 2, all from 1, all from 2, 1
not 2, 2 not 1, 1 xor 2

References
Agraﬁoti, I., Arneodo, F., Collins, F., et al. 2012, From the Geosphere to the
Cosmos, Synergies with Astroparticle Physics, Astroparticle Physics for
Europe (ASPERA), Contributed Volume, http://www.aspera-eu.org
Annis, J. T. 2014, in AAS Meeting 221, 335.05
Becciani, U., Bandiera, M., Brescia, M., et al. 2015, in Proc. ADASS
XXV Conf., Advanced Environment for Knowledge Discovery in the
VIALACTEA Project, in press (arXiv:1511.08619)
Benjamin, R. A., Churchwell, E., Babler, B. L., et al. 2003, PASP, 115, 953
Boch, T., Pineau, F. X., & Derriere, S. 2014, CDS xMatch Service
Documentation, http://cdsxmatch.u-strasbg.fr/xmatch/doc/
Braun, R. 2015, in Proc. Of The Many Facets of Extragalactic Radio Surveys:
Towards New Scientiﬁc Challenges (EXTRA-RADSUR2015) (Bologna:
SISSA), 34, http://pos.sissa.it/cgi-bin/reader/conf.cgi?confid=267

Budavári, T., & Lee, M. A. 2013, Xmatch: GPU Enhanced
Astronomic Catalog Cross-Matching, Astrophysics Source Code Library,
ascl:1303.021
Budavári, T., & Szalay, A. S. 2008, ApJ, 679, 301
Cavuoti, S., Brescia, M., & Longo, G. 2012, Proc. SPIE, 8451, 845103
Churchwell, E., Babler, B. L., Meade, M. R., et al. 2009, PASP, 121, 213
de Jong, J. T. A., Verdoes Kleijn, G. A., Boxhoorn, D. R., et al. 2015, A&A,
582, A62
Douglas, J., de Bruijne, J., O’Flaherty, K., et al. 2007, ESAABu, 132, 26
Du, P., Ren, J. J., Pan, J. C., & Luo, A. 2014, SCPMA, 57, 577
Gorski, K. M., Hivon, E., Banday, A. J., et al. 2005, ApJ, 622, 759
Gray, J., Nieto-Santisteban, M. A., & Szalay, A. S. 2006, The Zones Algorithm
for Finding Points-Near-a-Point or Cross-Matchin Spatial Datasets,
Microsoft Tech. Rep. MSR-TR-2006-52, http://www.microsoft.com/en-
us/research/wp-content/uploads/2006/04/tr-2006-52.doc
Gray, L. 2003, Not. Amer. Math. Soc., 50, 200, http://www.agsm.edu.au/
bobm/teaching/SimsSS/Fea-Gray.pdf
Ivezic, Z. 2009, in APS April Meeting Abstracts, LSST: the physics of the dark
universe, 54, W4.003
IVOA Recommendation 2005, An IVOA Standard for Uniﬁed Content
Descriptors Version 1.1
Jia, X., & Luo, Q. 2016, in Proc. 28th Int. Conf. on Scientiﬁc and Statistical
Database Management (SSDBM 16). Multi-Assignment Single Joins for
Parallel Cross-Match of Astronomic Catalogs on Heterogeneous Clusters,
ed. B. Peter et al. (New York, NY: ACM), 12
Jia, X., Luo, Q., & Fan, D. 2015, in Proc. IEEE XXI Int. Conf. on Parallel and
Distributed Systems (ICPADS) Cross-Matching Large Astronomic
Catalogs on Heterogeneous Clusters, 617
Kaiser, N. 2004, Proc. SPIE, 5489, 11
Kunszt, P. Z., Szalay, A. S., & Thakar, A. R. 2001, in Mining the Sky,
Proc. of MPA MPE Workshop, The Hierarchical Triangular
Mesh, ed. A. J. Banday, S. Zaroubi, & M. Bartelmann (Berlin:
Springer), 631
Laureijs, R., Raccu, G., Stagnaro, L., et al. 2014, Proc. SPIE, 9143,
91430H
Lee, M. A., & Budavári, T. 2013, in ASP Conf. Ser. 475, Proc. Astronomical
Data Analysis Software and Systems XXII Conf., Cross-Identiﬁcation of
Astronomical Catalogs on Multiple GPUs, ed. D. N. Friedel (San Francisco,
CA: ASP), 235
Lucas, P. W., Hoare, M. G., Longmore, A., et al. 2008, MNRAS,
391, 136
Malkov, O., Dluzhnevskaya, O., Karpov, S., et al. 2012, BaltA, 21, 319
Martins, C. J. A. P., Leite, A. C. Ó., & Pedrosa, P. O. J. 2015, in Proc.
IAU Symp. 306, Statistical Challenges in 21st Century Cosmology,
Fundamental Cosmology with the E-ELT, ed. A. Heavens,
J.-L. Starck, & A. Krone-Martins (Cambridge: Cambridge Univ Press), 385
Morlini, S., Schisano, E., Elia, D., et al. 2016, A&A, 591, A149
Mouch, C. & Arches Consortium 2015, in Proc. Astronomical Data Analysis
Software and Systems XXIV Conf., ed. A. R. Taylor & E. Rosolowsky
(San Francisco, CA: ASP), 437
Nieto-Santisteban, M. A., Thakar, A. R., & Szalay, A. S. 2006, Cross-
Matching Very Large Datasets (Baltimore, MD: Johns Hopkins Univ.)
Pineau, F. X., Boch, T., & Derriere, S. 2011, in ASP Conf. Ser. 442,
Astronomical Data Analysis Software and Systems XX, ed. I. N. Evans
et al. (San Francisco, CA: ASP), 85
Riccio, G., Brescia, M., Cavuoti, S., et al. 2016, Command-line Catalog
Crossmatch for modern astronomical surveys, Astrophysics Source Code
Library, ascl:1610.006
Sciaccà, E., Vitello, F., Becciani, U., et al. 2016, Proc. 8th Int. Workshop on
Advise Science Gateways, Milky Way analysis through a Science Gateway:
Workflows and Resource Monitoring, submitted
Taylor, M. B. 2005, in ASP Conf. Ser. 347, Astronomical Data Analysis
Software and Systems XIV, ed. P. Shopbell, M. Britton, & R. Ebert
(San Francisco, CA: ASP), 29
Taylor, M. B. 2006, in ASP Conf. Ser. 351, Astronomical Data Analysis
Software and Systems XV, ed. C. Gabriel et al. (San Francisco, CA: ASP), 666
