Quantum spin state selectivity and magnetic tuning of ultracold chemical reactions of triplet alkali-metal dimers with alkali-metal atoms

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We demonstrate that it is possible to efficiently control ultracold chemical reactions of alkali-metal atoms colliding with open-shell alkali-metal dimers in their metastable triplet states by choosing the internal hyperfine and rovibrational states of the reactants as well as by inducing magnetic Feshbach resonances with an external magnetic field. We base these conclusions on coupled-channel statistical calculations that include the effects of hyperfine contact and magnetic-field-induced Zeeman interactions on ultracold chemical reactions of hyperfine-resolved ground-state Na and the triplet NaLi(\(a^3\Sigma^+\)) producing singlet Na\(_2\)(\(1\Sigma^+\)) and a Li atom. We find that the reaction rates are sensitive to the initial hyperfine states of the reactants. The chemical reaction of fully spin-polarized, high-spin states of rotationless NaLi(\(a^3\Sigma^+, v = 0, N = 0\)) molecules with fully spin-polarized Na is suppressed by a factor of 10-100 compared to that of unpolarized reactants. We interpret these findings within the adiabatic state model, which treats the reaction as a sequence of nonadiabatic transitions between the initial non-reactive high-spin state and the final low-spin states of the reaction complex. In addition, we show that magnetic Feshbach resonances can similarly change reaction rate coefficients by several orders of magnitude. Some of these resonances are due to resonant trimer bound states dissociating to the \(N = 2\) rotational state of NaLi(\(a^3\Sigma^+, v = 0\)) and would thus exist in systems without hyperfine interactions.

Introduction. Recent experimental advances in molecular cooling and trapping have opened up new avenues of research into controlling chemical reactivity with external electromagnetic fields [1–3], the idea that fascinated scientists for decades, and led to the development of new research frontiers at the interface of chemistry and physics, such as mode-selective chemistry [4, 5], quantum coherent control [6], and attochemistry [7]. In particular, the production and trapping of ground-state molecular radicals NaLi(\(a^3\Sigma^+\)), Li\(_2\)(\(a^3\Sigma^+\)), Rb\(_2\)(\(a^3\Sigma^+\)), SrF(\(2\Sigma^+\)), CaF(\(2\Sigma^+\)), Yo(\(2\Sigma^+\)), YbF(\(2\Sigma^+\)) [8–14] and studies of their collisional properties at \(\mu\)K temperatures [15–18] suggested the possibility of using the reactant’s electron spin degrees of freedom to tune ultracold reaction dynamics by magnetic fields.

The prospect of using magnetic fields as a tool to control chemical reactivity is central to ultracold chemistry [1, 2] and a very important one in chemical kinetics [19] and biological magnetoreception [20], where radical pair reactions in cryptochrome proteins are thought to play a key role in magnetic-field-guided orientation of birds and insects [21, 22]. However, despite the long-standing significance of this question and the recent experimental observations of inelastic collisions in an ultracold Na-NaLi(\(a^3\Sigma^+\)) mixture [18], no theoretical studies have been reported on ultracold reaction dynamics involving ground-state alkali-metal dimers and atoms in the presence of external magnetic fields and hyperfine interactions. This is because such reactions occur through the formation of a deeply bound reaction complex [23–25], whose numerous strongly coupled bound and resonance states defy rigorous quantum scattering calculations [24–26].

Here, we explore the dynamics of the ultracold chemical reaction \(\text{Na} + \text{NaLi}(a^3\Sigma^+) \rightarrow \text{Na}_2(1\Sigma^+) + \text{Li}\) in the presence of magnetic fields and hyperfine interactions using the extended coupled-channel statistical (CCS) model [27] parametrized by ab initio calculations. The model assumes the existence of a long-lived reaction complex at short range, whose properties can be modeled statistically (i.e. using classical probabilities) [28–30]. Statistical (or universal) models [28–42] have been successfully applied to calculate the rate of ultracold chemical reactions of alkali-metal dimers [32, 34–36, 39] and the density of states of the (K\(_3\))\(_2\) reaction complex [43]. However, the previous calculations have been limited to the case of zero magnetic field and did not account for electron spins, hyperfine interactions, and non-adiabatic effects, all of which we will consider in the present work.

Our calculations show that the fully spin-polarized spin states of NaLi and Na are \(\sim 10\)-100 times less chemically reactive than unpolarized spin states, demonstrating extensive quantum spin state control of chemical reactions of triplet-state alkali-metal dimers with alkali-metal atoms. We also find that the magnetic field dependence of the reaction rate displays several magnetic Feshbach resonances (MFRs), providing the first theoretical prediction of MFRs in an ultracold chemical reaction. MFRs in non-reactive scattering of NaK with K were observed experimentally and thoroughly analysed in Refs. [44–46]. Our findings open up several new avenues of research in ultracold molecular physics and chemistry. The reactive MFRs will enable experimentalists to efficiently suppress unwanted chemical reactivity in trapped atom-molecule mixtures, enabling, e.g., effi-
cient sympathetic cooling [18, 47–52]. They could also be used to assemble chemically reactive atom-molecule trimers via magnetoassociation, to engineer entangled many-body states in trapped atom-molecule mixtures, and to probe and control the quantum dynamics of chaotic scattering and reaction complex formation [24].

**Theory: Ab initio calculations and extended CCS model.** To describe ultracold reactive collisions between Na atoms and NaLi molecules in the metastable \(a^3\Sigma^+\) electronic state, we performed *ab initio* calculations of the electronic potential energy surfaces (PESs) of the long-lived intermediate \(Na_2Li\) reaction complex. The complex is characterized by two \(2^A'\) and one \(4^A'\) trimer electronic states. The potential landscape of these barrierless PESs is shown in Fig. 1. The PESs are expressed in the Jacobi coordinates \(R\) — the atom-molecule separation vector and \(r\) — the vector joining the nuclei of the diatomic molecule. For our purposes it is sufficient to determine the PESs, which are only functions of \(R\) and \(\theta\) (the angle between \(R\) and \(r\)) in the two-dimensional plane with the internuclear distance of NaLi fixed at its equilibrium value \((r = r_e)\) [27]. Our *ab initio* calculations of the two-state \(2^A'\) PESs reveal a conical intersection (CI) between the two doublet states which is located at \(R \approx 8.5a_0\) and \(\theta = 70^\circ\). The relevant multi-dimensional PESs have been determined using the internally-contracted multi-reference configuration interaction (MRCI) method [53] with single and double excitations and Davidson correction [54] as further described in the Supplemental Material [55].

From the energetics of the relevant molecular states in the entrance and exit reaction channels we determine that the production of the \(Na_2(a^3\Sigma_u^+)\) molecule in the Na\((2S) + NaLi(a^3\Sigma^+)\) reaction is endothermic by 41.7 cm\(^{-1}\) including the zero-point vibrational energy correction. This suggests that the vibrational excitation of the reactant NaLi\((a^3\Sigma^+)\) molecule to the \(v \geq 2\) vibrational states will allow for production of triplet-state \(Na_2\) products. However, the CI allows for an efficient transfer of the reactant NaLi\((a^3\Sigma^+)\) molecules into either NaLi \((X^1\Sigma^+)\) or \(Na_2(X^1\Sigma^+)\) states of the ground electronic configuration. A schematic depiction of reactive scattering between Na atoms and NaLi\((a^3\Sigma^+)\) molecules through a CI is demonstrated in Fig. 1(a). The reactants start out on the asymptotically degenerate \(2^2A'\) and \(1^4A'\) excited PESs. The reaction flux on the \(2^2A'\) PESs can reach the CI and make a transition to the ground \(2^2A'\) PES leading to ground-state reaction products. Only the \(2^2A'\) and \(1^4A'\) PESs are included in our CCS calculations, which is justified by the fact that the CI is located deeply inside the reaction complex region not explicitly included in the calculations [55].

The extended CCS model of barrierless chemical reactions [27] assumes the existence of a long-lived reaction complex, whose formation from the reactants or decay to products can be treated as independent events [28, 29]. The state-to-state reaction probability between the reactant and product states \(r\) and \(p\) is given by the energy-dependent capture probabilities of the reactants and products into the reaction complex obtained by solving the time-independent Schrödinger equation in the entrance reaction channel subject to a short-range capture boundary condition for the reactive \(2^2A'\) PES and a regular boundary condition for the nonreactive \(4^A'\) PES [27, 55].

*Ultracold reaction dynamics in a magnetic field.** We begin by describing the hyperfine energy level structure of the reactants in a magnetic field. Figures 2(b) and (c) show the Zeeman levels of Na and NaLi\((a^3\Sigma^+, v = 0, N = 0)\) obtained by diagonalization of the atomic and molecular Hamiltonians [55]. There are a total of 36 molecular energy levels in the \(N = 0\) manifold of NaLi\((a^3\Sigma^+)\), which can be classified in the weak-field limit by the values of the total angular momentum of the molecule \(F\) and its projection on the field axis \(M_F\) [56, 57]. The calculated zero-field hyperfine splittings
are in good agreement with the measured values [8, 55].

To explore the influence of reactant spin polarization on chemical reactivity, we consider reactive collisions of NaLi molecules in the highest-energy level (36) of the $N = 0$ manifold with Na atoms in the hyperfine states [7] and [8] [see Figs. 2(b) and (c)]. Note that state [36] is a triply spin-polarized state of NaLi, where all of the spins in the molecule are aligned along the magnetic field. Similarly, state [8] of Na is doubly spin-polarized ($|F = 2, m_F = 2\rangle$), in contrast to state [7]. In the absence of the hyperfine structure, the Zeeman states of NaLi and Na shown in Fig. 2 reduce to 3 molecular states $|S_A M_{S_A}\rangle (M_{S_A} = 0, \pm 1)$, and 2 atomic states $|S_B M_{S_B}\rangle (M_{S_B} = \pm 1/2)$. The fully spin-polarized initial states of Na and NaLi are labeled as [2] and [3].

In Fig. 2(a) we plot the magnetic field dependence of the reaction rates for the (8,36) and (7,36) initial states of Na + NaLi at $T = 2 \mu K$. The rates are nearly temperature independent, as expected for a two-body inelastic process near an s-wave threshold [58].

More significantly, we observe that the chemical reactivity of fully spin-polarized reactants Na(8) + NaLi(36) is suppressed by a factor of $\approx 10$-100 compared to that of non-fully spin-polarized reactants Na(7) + NaLi(36). Remarkably, flipping the electron spin of one of the reactants leads to a dramatic change in chemical reactivity. While the strong dependence on the initial spin state has been observed previously for Penning ionization in cold atom-atom collisions [59], the atom-molecule reaction studied here is essentially different due to the large number of participating rovibrational states coupled by strongly anisotropic atom-atom interactions.

The rate of the Na(7) + NaLi(36) reaction displays the opposite trend, beginning to decrease at $B \geq 0.05$ T. This trend is similar to that observed in [27] and can be explained by referring to Eq. (1): the weight $c_2(B)$ of the "reactive" electron spin state $|1/2, -1/2\rangle$ in the hyperfine state [7] of Na

$$|7\rangle = c_1(B)|1/2, 1/2\rangle + c_2(B)|1/2, -1/2\rangle$$

is the Boltzmann constant. The initial state of the reaction complex is initialized in the nonreactive state of total spin $S = 3/2$ described by the $^4A'$ PES (see Fig. 1). Thus, in the absence of S-nonconserving interactions, such as the intramolecular spin-spin or intermolecular magnetic dipole interactions, the value of $S$ must be the same for the reactants and products (the Wigner spin rule [60]). The energetically allowed products of the Na + NaLi reaction—molecular Na$_2$(1$\Sigma^+$) and atomic Li($^2S_{1/2}$) —correspond to $S = 1/2$. As a result, the spin-polarized chemical reaction Na + NaLi($a^3\Sigma^+$) $\rightarrow$ Na$_2$(1$\Sigma^+$) + Li requires spin-changing intersystem crossing transition $S = 3/2 \rightarrow 1/2$ [63–67] in order to proceed. We verified that omitting the spin-spin and magnetic dipolar interactions from CCS calculations leads to a complete suppression of the reaction Na(8) + NaLi(36) $\rightarrow$ Na$_2$ + Li, while having little ef-
fect on the reactivity of the initial state (7,36).

To gain further insight into the mechanism of the spin-polarized chemical reaction \( \text{Na} + \text{NaLi}(a^3\Sigma^+) \) we plot in Fig. 3(a) the adiabatic eigenvalues \( \epsilon_i(R) \) of the atom-molecule Hamiltonian [31, 33, 68–70]. Consider, e.g., the \( S = 3/2 \) diabatic potential obtained by following the corresponding adiabatic curves through a series of avoided crossings shown in Fig. 3. The potential is repulsive at short range with a well depth of \( \approx 200 \text{ cm}^{-1} \), and correlates with the fully spin-polarized initial state of Na(2)-NaLi(3). The repulsive state experiences several crossings with the \( S = 1/2 \) diabatic states, which are attractive at short range and correlate asymptotically with unpolarized rotationally excited states of NaLi. The crossings are induced by \( S \)-nonconserving interactions, predominantly by the intramolecular spin-spin interaction of NaLi(\( a^3\Sigma^+ \)) which cause the chemical reaction. We note that a simple two-channel model involving the pair of diabatic states near the largest avoided crossing shown in Fig. 3(b) underestimates the reaction rate by several orders of magnitude (as does Landau-Zener theory), suggesting the importance of multichannel effects.

The resonance variation of the spin-polarized reaction rate near \( B = 0.4 \text{ T} \) shown in Fig. 2(a)

is caused by MFRs, which occur due to the coupling of the incident spin-polarized channel \( |N_A = 0, M_{S_A} = 1 \rangle \) with closed-channel bound states \( |N_A = 2, M_{S_A} \rangle (M_{S_A} \neq M_{S_A}) \) mediated by \textit{anisotropic interactions}, which include the intramolecular spin-spin interaction of NaLi(\( a^3\Sigma^+ \)) [71] and the anisotropic part of the Na-NaLi interaction. The near-threshold bound state responsible for the MFR at \( 0.42 \text{ T} \) is supported by the adiabatic potential that correlates to the \( |N_A = 2, M_{S_A} = 0 \rangle |M_{S_B} = -\frac{1}{2} \rangle \) closed-channel threshold, as shown in Fig. 3(c).

Figure 3(c) illustrates that MFRs can also occur in the spin-unpolarized incident channel (1,3). The low-field resonance is mainly due to the atom-molecule interaction anisotropy, which couples the \( N = 0 \) incident channel with \( N > 0 \) closed channels. Indeed, as shown in Fig. 3(e) the MFR disappears when the anisotropic part of the Na-NaLi interaction is omitted.

Our calculated Na-NaLi reaction rates deviate substantially from the universal value \( k_0^u = 1.84 \times 10^{-10} \text{ cm}^3/\text{s} \) [72, 73] calculated using the accurate \textit{ab initio} Na-NaLi(\( a^3\Sigma^+ \)) long-range dispersion coefficient \( C_6 \) of 4026 a.u. [55]. This indicates a substantial degree of non-universality due to the inherently multichannel nature of the reaction dynamics caused by anisotropic interactions (see above). As shown in Fig. 3(a) a large fraction of adiabatic channels, through which the reaction occurs, is repulsive at short range, leading to a significant reflection of the incident flux even for unpolarized initial reactant states. This reflection manifests in the appearance of MFRs and other non-universal effects [72]. Test calculations show that in the absence of anisotropic interactions, the unpolarized reaction rate remains close to the universal limit over the entire range of magnetic fields [see Fig. 3(e)].

In summary, we have presented a theoretical study of the ultracold chemical reaction of Na atoms with triplet NaLi(\( a^3\Sigma^+ \)) molecules in their ground rovibational states in the presence of external magnetic fields and hyperfine interactions. This reaction is represen-
tative of a wide class of ultracold chemical reactions of triplet alkali-dimer molecules currently studied by several experimental groups [15, 16, 18]. Our calculations reveal a substantial degree of quantum state selectivity in the dependence of the reaction rate on the initial states of the reactants (fully spin-polarized vs. unpolarized). Our results also suggest that it is possible to control ultracold chemical reactions of alkali-metal dimers with alkali-metal atoms via magnetic Feshbach resonances.

The generality of the spin-based control mechanisms explored here implies their potential utility as a tool to control other, potentially more complex chemical reactions, such as those of heavier bialkali molecules [e.g., K + KRb(a3Σ)] and those involving 2Σ molecules, such as Li + CaH(2Σ) [27, 48], Li + SrOH(2Σ) [49], and Li + CaF(2Σ) [51]. We thus expect our results to be tested in near-future experiments with ultracold atom-molecule mixtures.

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