Conductive nitrides: Growth principles, optical and electronic properties, and their perspectives in photonics and plasmonics

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The nitrides of most of the group IVb-Vb-VIb transition metals (TiN, ZrN, HfN, VN, NbN, TaN, MoN, WN) constitute the unique category of conductive ceramics. Having substantial electronic conductivity, exceptionally high melting points and covering a wide range of work function values, they were considered for a variety of electronic applications, which include diffusion barriers in metallizations of integrated circuits, Ohmic contacts on compound semiconductors, and thin film resistors, since early eighties. Among them, TiN and ZrN are recently emerging as significant candidates for plasmonic applications. So the possible plasmonic activity of the rest of transition metal nitrides (TMN) emerges as an important open question. In this work, we exhaustively review the experimental and computational (mostly ab initio) works in the literature dealing with the optical properties and electronic structure of TMN spanning over three decades of time and employing all the available growth techniques. We critically evaluate the optical properties of all TMN and we model their predicted plasmonic response. Hence, we provide a solid understanding of the intrinsic (e.g. the valence electron configuration of the constituent metal) and extrinsic (e.g. point defects and microstructure) factors that dictate the plasmonic performance. Based on the reported optical spectra, we evaluate the quality factors for surface plasmon polariton and localized surface plasmon for various TMN and critically compare them to each other. We demonstrate that, indeed TiN and ZrN along with HfN are the most well-performing plasmonic materials in the visible range, while VN and NbN may be viable alternatives for plasmonic devices in the blue, violet and near UV ranges, albeit in expense of increased electronic loss. Furthermore, we consider the alloyed ternary TMN and by critical evaluation and comparison of the reported experimental and computational works, we identify the emerging optimal tunable plasmonic conductors among the immense number of alloying combinations.

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1. Introduction

The recent emergence of plasmonics, the science and technology of metallic nanostructures interacting with light, is based upon the surface plasmon polariton (SPP) modes in planar surfaces and localized surface plasmon resonance (LSPR) in metallic nanoparticles [1–14], two unique phenomena that manifest exclusively at the nanoscale. As a result, plasmonics is one of the most characteristic examples of what is called ‘nanotechnology’ nowadays, despite being manifested since antiquity and theoretically explained since the early twentieth century [15,16]. Thus, plasmonics promise radical breakthroughs in electronic devices [17–24], biosensing [25–35], catalysis and photochemistry [36–45], solar energy harvesting [46–64], photodetection [65–74], optical storage of information [75–84], telecommunications [85–94] and metamaterials [95–99]. These applications are, in their turn, based on the high spatial resolution of SPP and LSPR, which is below the diffraction limit of light [7,82,100–103], the ultra-fast response of plasmonic systems [104–107], the maximized absorption and scattering of light [1,108], the creation of extreme near-fields [114–119] that result due to the partially filled valence orbitals that are not completely established [184,188–200]. They also exhibit electronic conductivity due to the partially filled valence d orbitals that are not completely hybridized 

In this work we review the fundamental properties (phases, microstructure, growth techniques) of the TMN, as well as their electronic structure via detailed ab-initio and semi-empirical computational methods, their dielectric function spectra extracted from an extended literature survey of reported ellipsometry and optical reflectivity spectra. As a result, we critically compare the reported electronic properties (such as resistivity/conductivity, conduction electron density-via the unscreened plasma energy, the spectral position of their interband transitions and their work-function). We also consider the effect of grain size to the optical and electronic properties of TMN.

Furthermore we consider the successful alloying of TMN to form ternary TMN (or more accurately pseudobinary nitrides, because the B1 structure is retained in the entire compositional range and the nitrogen sublattice of the B1 structure remains intact during
alloying) with tuned electronic properties [238–253]. We demonstrate that these ternary systems provide exceptional flexibility, vast range for the values of the main electronic properties, thus offering immense potential for applications in plasmonics.

Finally and most importantly, we evaluate the potential use of binary and ternary TMN as core components for plasmonics by providing the LSPR performance of TMN nanoparticles through detailed Maxwell-Garnett effective medium approximation calculations and accurate Finite Difference Time Domain (FTDT) calculations. We demonstrate that the plasmonic response of nanoparticles of TMN is equivalent to that of nanoparticles of noble metals. In addition, we show that TMN can be active and stable plasmonic materials with LSPR ranging from the UV (using TaN and Ta-rich Ti_{1-x}Ta_{x}N) to IR (using ternary Ti_{x}Sc_{1-x}N and Ti_{x}Al_{1-x}N) and combining additional assets such as refractory character, which makes them suitable for high temperature/high power plasmonics [182,183,254], photothermal applications [255], and low work function that makes them suitable for plasmon-enhanced electron emitters.

2. TMN continuous films

2.1. Fundamental features and growth

2.1.1. Fundamental features

2.1.1.1. Nitrides of group IVb elements (TiN, ZrN, HfN). The metals of the group IVb of the periodic table of elements have four valence electrons with a configuration of d^{2}s^{2} for all the three metals ([Ar]3d^{2}4s^{2}, [Kr]4d^{2}s^{2} and [Xe]4f^{14}5d^{6}s^{2} for Ti, Zr, and Hf, respectively) and they form bonds with N atoms (valence electronic configuration 2s 2p^{3}). While various nitride phases such as the Me_2N [256,257] and Me_3N_4 (Me = Ti, Zr, Hf) [258,259] were reported, the most stable and durable nitrides of these metals are those in the cubic rocksalt B1-MeN arrangement or also called 3-MeN (Me = Ti, Zr, Hf). The B1 TiN, ZrN and HfN are characterized by gold-like yellow color (bright yellow for TiN and becoming gradually paler for ZrN and HfN [184,190]), high hardness [188,196], electrical conductivity [184,226] and refractory character [198].

B1-TiN is the archetypical example of the conductive nitrides. It has been studied since the early 1930s and B1-TiN films have been systematically grown and studied since the mid-1970s [260]. B1-TiN is considered nowadays as one of the most technologically important materials. A wide variety of fabrication techniques have been used for the growth of B1-TiN films, such as Magnetron Sputtering (MS) [261–268], Cathodic Vacuum Arc (CVA) [269–271], Chemical Vapor Deposition (CVD) [272,273], Atomic Layer Deposition (ALD) [189], Pulsed Laser Deposition (PLD) [184,274], Ion Beam Assisted Deposition (IBAD) [275], Dual Ion Beam Sputtering (DBS) [276], and High Power Impulse Magnetron Sputtering (HIPIMS) [277]. The numerous works on the growth of B1-TiN led to an unprecedented understanding and control of its microstructural features, such as the grain size, orientation, columnar or globular type of growth, etc [276,278–282], and

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### Fig. 1

An excerpt of the periodic table of elements where the usual constituents of the various conductive binary and ternary transition metal nitrides are shown (blue and green are the usual constituent of the conductive nitrides of B1 structure, magenta are the elements that can be potentially used as dopants in order to control the conductivity and the LSPR spectral position and red are elements that are not recommended for electronic applications); data taken from [184–187]. The colors of the cells are a graphic indication of the color of light where LSPR can occur for nanoparticles of a ternary nitride of the form B1-Ti_{x}E_{1-x}N, where E is the corresponding element (dark wine color stands for infrared). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

![Periodic Table Excerpt](image-url)
electron configurations are \([\text{Ar}]3d^44s^2, [\text{Kr}]4d^55s^1,\) and \([\text{Xe}]5d^46s^2,\) consequently they have six valence electrons and their valence have one more valence electron than Ti, Zr, and Hf, respectively.

2.1.1.3. Nitrides of group VIb elements (CrN, MoN, WN). Cr, Mo and W have one more electron than V, Nb, and Ta, respectively, consequently they have six valence electrons and their valence electron configurations are \([\text{Ar}]3d^44s^2, [\text{Kr}]4d^45s^5,\) and \([\text{Xe}]5d^56s^2,\) respectively. VN and NbN can form easily the B1 nitride phase while B1-TaN is metastable. Several techniques were used for their growth, such as reactive sputter deposition (VN [330–333], NbN [334], TaN [335–340]), CVA (NbN [341–343], TaN [344]), PLD (VN [345], NbN [184,200,346,347], TaN [184,200,274]), ALD (VN [348,349], NbN [188,350], TaN [188,351,352]), CVD (VN [353], NbN [191], TaN [191,353]), and IBAD (VN [354], NbN [355], TaN [356]). The epitaxial growth of B1-VN, B1-NbN and less frequently of B1-TaN, mostly on MgO, was also achieved successfully [333,357–360]. According to Papaconstantopoulos et al. [361] B1-VN, B1-NbN, B1-TaN are paramagnetic, while they all have been reported to be superconductors [347,362]. Especially NbN is a well known superconductor whose superconducting properties have been under investigation since the early 1980s [216–218,363–368]. B1-VN, B1-NbN, B1-TaN have also remarkable mechanical properties and stability and were studied accordingly [188,369–376], though not so intensively as B1-TaN and B1-ZrN.

Among them, TaN was more intensively studied, especially regarding its electrical properties, which are relevant to applications as diffusion barrier [202–205,209,377] and metallizations [196,225,228,233,378,379] where TaN is becoming an industry-standard material. B1-TaN has a colorless grayish appearance and its optical properties have been thoroughly investigated [168,169,174,184,200,242,246,248,251,380–383] and can be tuned by alloying with TiN, [184,246,248,251] or ZrN [242]; due to its remarkable optical properties, it was proposed as a promising alternative plasmonic material [168,169,174]. Note however, that TaN is very hardly stabilized in the B1 phase [376,384], although high quality B1-TaN has been achieved by few authors [381,385,386], and it has been recently suggested that the point defects, which are undesirable for the electrical conductivity, are playing a crucial role towards the stability of B1-TaN [387].

Studies on the optical properties of VN [238,328,380,388] and NbN do exist [184,200,389–391] but they are far more rare.

2.1.1.3. Nitrides of group Vb elements (CrN, MoN, WN). Cr, Mo and W have one more electron than V, Nb, and Ta, respectively, consequently they have six valence electrons and their valence electron configurations are \([\text{Ar}]3d^34s^2, [\text{Kr}]4d^45s^5,\) and \([\text{Xe}]5d^56s^2,\) respectively. Cr can easily form the B1 nitride phase by conventional sputtering [392–395], HIPIMS [277,396,397], MBE [398], and CVD [399]. The attention that B1-CrN received was due to its superior wear and anti-corrosion performance compared to B1-TiN [400–408]. The magnetic properties of CrN are unique among all the TMN, as implied since the pioneering work of Papaconstantopoulos [361] where the paramagnetic state of CrN was questioned, and clearly proven by Filippetti et al. who performed spin polarized calculations and predicted its semiconductor-like character when in anti-ferromagnetic state [409]. The interplay between the magnetic properties of CrN and its semiconductor behavior was experimentally confirmed by several groups [408,410–412] and disregard it as a candidate plasmonic conductor; therefore, the study of its electronic structure and dielectric function spectra is excluded from this work.

B1-MoN and B1-WN are the less studied among all TMN, MoN has been studied since early 1980s [413]. It is hardly stabilized in the

![Fig. 2.](image-url)
B1 structure and competitive hexagonal MoN phases exist [414,445]. MoN is also paramagnetic [361] and superconducting [416–418]. B1-MoN has been reported to be grown by sputtering [414,449], PLD [184,200], CVA [420], IBAD [421], CVD [422,423], and ALD [424]. WN was considered mostly as a diffusion barrier [425] and despite of being deposited by a variety of techniques, such as sputtering [211,370,426,427], CVD [422,428], and ALD [429,430] its B1 phase in epitaxial form on MgO and sapphire has been very recently achieved [187]. Consequently, the studies of their optical properties are extremely rare [184,200,431], while until recently [184,432] the optical properties of B1-WN were missing from the literature, since most of the reported works dealing with WN refered to other phases.

Both MoN and WN are unstable in the B1 cubic structure [186,387,433] and it was recently revealed that the existence of point defects (metal and ligand vacancies) play a crucial role for their stabilization [186,387,433].

2.1.4. Ternary conductive nitrides. Alloying the aforementioned TMN to form ternary (or more accurately pseudo-binary) films is an effective pathway to controlling their mechanical, optical and electronic properties. The similar crystal structure (rocksalt), local symmetry (octahedral) and the similar bonding to N (via hybridization of the metal’s $d$ electrons with the nitrogen’s $2p$ electrons) [187], make all the nitrides of the group IVb, VB, and VIb metals completely soluble to each other in the B1 phase and in the entire compositional range [184,249,250]; in fact, such alloying may result in more stable films with less structural defects compared to some metastable binary nitrides, with the most prominent example being the stable Ta-rich B1-Ti$_{1-x}$Ta$_x$N and the metastable B1-TaN [376]. The most widely used alloying phase for electronic applications is the B1-TiN, which is implemented as the basis for the formation of Ti$_x$Zr$_{1-x}$N [251,305,376], Ti$_x$Hf$_{1-x}$N [184,249], Ti$_x$V$_{1-x}$N [238,247,253], Ti$_x$Nb$_{1-x}$N [184,249,250], Ti$_x$Ta$_{1-x}$N [376,434], Ti$_x$Cr$_{1-x}$N [241], Ti$_x$Mo$_{1-x}$N [184,239,241,249,250,435,436], and Ti$_x$W$_{1-x}$N [184,437,438].

Electronics-relevant Ta-based (Ta$_x$Zr$_{1-x}$N and Ta$_x$W$_{1-x}$N) [184,242,244,249,250,439], Zr-based (Zr$_x$Hf$_{1-x}$N, Zr$_x$Nb$_{1-x}$N, Zr$_x$Cr$_{1-x}$N, Zr$_x$Y$_{1-x}$N) [243,245,440,441], and V-based (V$_x$W$_{1-x}$N) [370] ternary nitrides were also reported.

Apart from the structural stability, the driving force for alloying and forming ternary conductive nitrides is the tailoring of key properties, such as the resistance against oxidation that enhances the stability and lifetime of the films [442], the diffusion barrier capability [443], the electrical resistivity [248,251,444], the work function [184,445], the superconductivity [446,447], the optical reflectivity edge, which defines the color and brightness of optical films [184,448], and more recently the conduction electron density, which defines the plasmonic response of nanoparticles of these nitrides [439].

Ti, Zr, and Hf share the same valence electron configuration of the constituent metal ($d^2s^2$) and they form bonds with nitrogen atoms (valence electron configuration $2s^22p^3$). Their electrical conductivity is due to the excess of $d$ electrons of the metal. By substituting any of these metal atoms by atoms of a group Vb (V, Nb, Ta) or group Vb (Mo, W) element, the cubic ternary structure is enriched with conduction electrons [184], thus increasing the resistivity [248], and blueshifting the reflectivity edge [184,200,434] and the localized surface plasmon resonance of the corresponding nanoparticles [439].

It is clear that such alloying cannot reduce the conduction electron density below that of B1-TiN and B1-ZrN and B1-HfN. In order to reduce their conduction electron density, and shift their optical and plasmonic performance towards the infrared, B1-TiN and B1-ZrN should be alloyed with group III or II elements. Among the group IIIa elements the only efficient candidate for alloying with B1-TiN and B1-ZrN is Al (valence electron configuration $3s^23p^1$). Despite of AlN being mostly crystallized in the wurzite-type hexagonal phase w-AlN and being a well-known extremely wide band gap semiconductor ($E_g = 6.2$ eV) [449–452], Al can be incorporated as an alloying element into Ti substitutional positions in B1-TiN and form the pseudobinary alloy B1-Ti$_x$Al$_{1-x}$N [198,439,453–457]. The B1-Ti$_x$Al$_{1-x}$N phase is electrically conductive and stable only in the range $0.55 < x < 1$; its electrical and optical properties are apparently varying with $x$ [453,457–460]. Electronic and photonic applications of the Ti$_x$Al$_{1-x}$N system include decorative colored coatings [453], plasmonic conductors operating in the deep red [439] and solar selective absorbers [461]. For the time being, the rest of the group IIIa elements are not efficient in alloying with B1-TiN. Ti-B-N films tend to be nanocomposite, and not ternary or pseudo-binary compounds, due to the competition of the rocksalt TiN and the hexagonal TiB$_2$ phases [462,463] and resemble more the properties of the Ti-Si-N nanocomposites [464]. Ti$_x$Ga$_{1-x}$N is extremely scarce [461] due to the incompatibility of the sputtering process used for the TiN growth and the MBE process used for the GaN growth [465]; note that gallium targets cannot endure the plasma in the sputtering process and liquefy due the exceptional low melting point of gallium [465]; the emergence of the ALD technology for the growth of both TiN and GaN [467,468] can overcome the process incompatibility and might enable in the future the elaboration of these alloys and the more careful investigation of this compound. Finally, indium combines the drawbacks of gallium in alloying with B1-TiN with the large mismatch of the atomic radii of titanium and indium, which are expected to induce severe stress and a strong driving force for decomposition; consequently, there is no report for the formation of Ti$_x$In$_{1-x}$N.

As Al is not soluble in B1-TiN in the entire compositional range, other candidate substitution elements with three or two valence electron, such as the rare earth elements (Sc, Y, La) of group IIIb and the alkaline earth elements (Mg, Ca) of group II have been considered, and Ti$_x$Sc$_{1-x}$N, Ti$_x$Y$_{1-x}$N, Zr$_x$Y$_{1-x}$N, Ti-La-N (amorphous), Ti$_x$Mg$_{1-x}$N and Ti$_x$Ca$_{1-x}$N films were reported [441,469–472]. Among them, the most promising in terms of its electronic and optical properties, as well as of its stability, is Ti$_x$Sc$_{1-x}$N [441,469,471]. This is mostly due to the valence electron configuration (3$d^4$4$s^2$) of Sc, and the B1 crystal structure being the most stable phase of ScN, which is, however, an intermediate bandgap semiconductor ($E_g = 1.30–1.58$ eV) [473–476]. As a direct consequence of the similar crystal structure (B1) and valence electron configuration (partially filled $d$-band added filled $s$-band) of ScN and TiN, the pseudobinary B1-Ti$_x$Sc$_{1-x}$N is stable in the B1 structure in the entire compositional range ($0 < x < 1$) and films of exceptionally high crystallinity and outstanding optical performance can be achieved [441,469–471].

2.1.2. Growth mechanisms, structural defects and stress, strain development

The high melting point of TMN has the direct consequence of their usual fine crystal structure and the ability of growing high crystalline quality TMN has been a subject of intense research for several years. In addition, it has been recently suggested [439,441] that the crystallinity of such films is of paramount importance for their plasmonic behavior. As a result, reviewing the growth mechanisms, microstructure and stress development during physical vapor deposition (PVD) of TMN thin films is very important for the understanding of TMN and for their critical evaluation for realistic applications in photonics and plasmonics. A special emphasis is given to TiN, which is the most widely studied binary compound among conductive TMN. We discuss the origin of stress evolution in binary and ternary compounds, based on recent kinetic stress models, as well as the growth-induced structural defects due to energetic particles impingement of the film surface/
subsurface that takes place under energetic deposition conditions, such as MS, DIBS, CVA, and HiPIMS. We will also illustrate the interplay between growth morphology, phase formation, texture and stress development for the case of ternary nitrides, for which a large variety of microstructures can be formed. Such microstructural attributes, in terms of grain size, preferential orientation and stress levels can deeply influence the TMN optical properties. The knowledge of these ‘extrinsic’ effects is as crucial as the ground electronic features of TMN for the quest in the design of conductive TMN for photonic and plasmonic applications.

2.1.2.1. Microstructural development during TiN film growth. A general development of film microstructure with respect to various growth conditions is commonly represented by diagrams called structure zone models (SZM) [477], which tend to relate the effects of the process parameters on the resulting microstructure of polycrystalline thin film materials. These diagrams are usually compiled as a function of the homologous temperature, $T_h = \frac{T_s}{T_M}$, where $T_s$ is the substrate temperature and $T_M$ is the melting point of the deposited material ($T_M = 3222$ K for TiN). For the case of sputter-deposition, it is also necessary to take into account the working pressure [478], and more generally the energy deposited per incident particle, $E_d$ [479]. Typical deposition conditions to obtain stoichiometric TiN films with a relatively dense microstructure require sufficient adatom mobility, i.e. operating at $T_s$ in the 550–800 K range, resulting in $T_h \sim 0.17–0.25$, which corresponds to microstructures of Zone T-type of SZM [480]. The microstructure of polycrystalline TiN films grown under Zone T consists of V-shaped columns [184,481] see Fig. 3a, characteristic of an evolutionary microstructure throughout the film thickness, i.e. the columns become larger at larger film thickness; such features are limited for films thinner than 100 nm, which are usually employed in photonic and plasmonic devices [224]. The bright contrast between columns in the cross-sectional TEM image of Fig. 3a corresponds to voided grain boundaries, and this effect is also more pronounced with increasing film thickness. These columns emerge at the surface forming facets, corresponding to crystallographic planes of low surface energy $\gamma$, resulting in rough surface morphologies. The planes of lowest $\gamma$ correspond to the planes with the largest lateral growth rate, in other words to the lowest perpendicular crystallographic growth rate. The formation of V-shaped columns is the result of a kinetically-limited competitive columnar growth, due to anisotropy in adatom surface diffusion: after random nucleation of grains [480], some column/grain orientations survive, while others disappear, and the film microstructure shown in Fig. 3a testifies that overgrowth has
occurred during film thickening. Mahieu et al. [477] have shown that the preferred orientation of TiN films grown under Zone-T corresponds to the geometrically fastest growing direction perpendicular to the substrate, i.e. the texture that develops corresponds to the [hkl]-oriented columns that gradually envelop and overgrow the other out-of-plane oriented grains. In this temperature range, the mobility is high enough to allow for surface diffusion as well as intergrain diffusion (mass transport from one grain to another), but not for bulk diffusion (grain boundary are immobile) so that restructuring is prohibited. The preferred orientation depends on the nature of the reactive gas species (either atomic N or N$_2$ molecule) and incoming adparticles (either Ti or TiN), which dictates the crystallographic orientation which forms the facets [480]. For conditions at which the formed facets are {100}, the fastest geometric growth direction is [111], and TiN films will have a [111] out-of-plane preferred orientation. The corresponding surface morphology consists of nicely faceted grains of tetrahedron shape, pointing with a corner upward (see Fig. 3b), typically obtained for MS at low N$_2$ partial pressure for which the forms the facets [480]. For conditions at which the formed facets correspond to zone T and finally to Zone II. Mahieu and Depla [268] suggested that the crossing from Zone T to Zone II involves recrystallization processes occurring through island ripening and island diffusion rather than by grain boundary migration. The close correlation between the magnitude of particle fluxes reaching the substrate, preferred orientation and microstructure is rationalized in terms of extended SZM [477] and also in line with the atomic N/ Ti flux model of Gall et al. [281]. Using ab initio calculations, these authors reported that in the presence of excess atomic N, the diffusion length of Ti adatoms is significantly reduced on (001) planes, leading to a lower chemical potential for Ti adatoms on (001) than on (111), $\mu_{Ti,001} < \mu_{Ti,111}$, and consequently to a net atomic flux from 111- to 001-oriented grains. This latter grain orientation will therefore survive under high N/Ti flux conditions. This might be an important pathway for the growth of low electron loss TiN at moderate temperatures.

Ion bombardment can often be used to enhance film densification. Several processes take place, including biased surface diffusion by momentum transfer, but also creation of primary recoils, followed by knock-on atomic displacement events and eventually defect formation in the subsurface once the energy of incoming particles exceeds the energy threshold for atomic displacement, $E_{\text{loss}}$, which is typically around 25 eV for Ti. The use of such hyperthermal particle fluxes will favor renucleation and restructuring, leading to a more fine-grained microstructure, but can be highly detrimental in terms of compressive stress that is generated by subplantation mechanism [282], as it will be discussed below.

Finally, the use of pulsed particle fluxes, as generated by HiPIMS discharges, modifies both the plasma composition and ionization degree of the metallic species. At high discharge currents (20–30 A), a significant fraction of metallic Ti$^+$, (J$_{Ti^+}$J$_{Ti}$ > 1) and Ti$^{2+}$, (J$_{Ti^{2+}}$, J$_{Ti}$ ~ 0.5) ions will reach the growing film surface, together with N$^+$ and N$^-$ ions coming from nitrogen dissociation in the plasma, thereby influencing nucleation, competitive columnar growth, column size, texture and stress state [442]. Note that N$^+$ ions with energy above the binding energy of molecular N$_2$ (9.7 eV) [484] will dissociate upon collision with the film surface.

2.1.2.2. Effect of deposition parameters on stress evolution in TiN thin films. The origin of the residual stress is in general associated with structural changes occurring during film growth (growth or intrinsic stress), the effect of post-deposition temperature change (thermal stress) and effects following growth (extrinsic stress). Typical processes resulting in the development of either tensile or compressive intrinsic stress comprise coalescence of crystallite islands in the initial growth stages, grain growth and corresponding reduction of volume fraction of grain boundaries, shrinkage of grain boundary voids, grain boundary relaxation, defect annihilation, incorporation of adatoms into grains and grain boundaries and incorporation of additives/impurities. Consequently, minimizing the electron loss in conductive nitrides requires the elimination of such defects and of the stress, which is a strong indicator for their existence. An understanding of the origin and development of stresses in thin films grown under various process conditions was recently possible due to real-time and depth-resolved analytical methods applied to deduce relations between fundamental film-forming processes, structural development and stress generating mechanisms [267,291,442,484]. Fig. 4a shows the evolution of the stress-thickness product ($\sigma$ x $h$) for a series of TiN films deposited by MS at different N$_2$ flows. Depending on the N$_2$ flow, and therefore N/Ti flux, the stress that develops can be either tensile (at low N$_2$) or compressive (at high N$_2$). It can be clearly observed that the stress evolves with film thickness, attesting for the presence of stress gradients along the film thickness. No steady-state stress is reached in the investigated film thickness range and this is associated with an evolutionary microstructure following a Zone T regime: the incremental stress (given by the derivative of $\sigma$ x $h$...
with respect to film thickness \( h \) is initially compressive, typically for \( h < 10 \) nm values of \(-3 \) GPa are obtained, and gradually levels off with increasing thickness or even becomes tensile \((+0.6 \text{ Pa})\) for TiN films deposited at low \( \text{N}_2 \) flow. The change from compressive

towards tensile regime occurring in the early growth stages is more clearly seen in Fig. 4b, where the effect of varying substrate bias voltage is additionally reported. By changing the bias voltage during the course of deposition the slope of the stress-thickness curves is altered, the incremental stress becoming less tensile when larger bias voltages are applied. This evidences that the intrinsic stress that develops in TiN films with Zone T microstructures is the sum of two competing sources: a compressive stress source due to attraction between columns and a compressive stress source due to energetic bombardment of the growing film. This latter effect is known as the “atomic peening” process, in which defects are created by energetic species. This occurs typically in the sub-surface region, when the energy of incoming particles exceeds the subplantation energy threshold, which is \( \sim 50 \text{ eV for TiN} \) \([282,485]\). Recent experimental findings have shown the importance of grain boundary on the mechanisms of defects incorporation during thin film growth \([486,487]\). The grain boundaries act as preferential sites for incorporation of excess atoms. Defects can also be created in the grain interior, in the form of vacancies, self-interstitials or substitutional atoms. The net result of the incorporation of interstitial-type defects or substitutional atoms with larger size than the host atoms is a volume expansion (associated with a hydrostatic stress field around the defect), which reduces the in-plane compressive stress state since the lateral dimensions of the film are fixed by those of the rigid substrate. Depending on the deposition rate, grain size, adatom surface diffusivity and energy of incoming species, complex stress variations are therefore anticipated. A kinetic stress model for PVD thin film growth under energetic conditions has been recently proposed \([488,489]\), to which the interested reader can refer more details.

At constant deposition conditions, the energetic bombardment in the growing film remains the same throughout the whole deposition, so any stress evolution is related to a change in microstructure/texture. Typically, for Zone T, as the columns enlarge with film thickening, the stress turns from compressive to tensile, which is a direct consequence of evolutionary nature of the microstructure (the fraction of grain boundary decreases from the substrate interface towards the film surface, see Fig. 3a). The correlation between stress gradients and column/grain size variations has been evidenced recently by Daniel et al. \([490,491]\) on TiN films using depth-sensitive X-ray nanodiffraction. By increasing the bias voltage during deposition, the energy of ions accelerated across the substrate sheath increases, which has the immediate consequence to increase the contribution of atomic peening, resulting in a less tensile incremental stress, as illustrated in Fig. 4b.

As discussed above, the degree of texture, grain size and surface morphology of TiN films grown by reactive MS can be tailored by appropriate choice of the deposition conditions, i.e. by monitoring the substrate temperature \( T_s \), the \( \text{N}/\text{Ti} \) flux or the average energy per deposited particles, \( E_d \). These parameters will also strongly impact the resulting stress state. The energetic species contributing to \( E_d \) are the film-forming species, backscattered gas neutrals (gas ions that are neutralized and reflected at the sputtering target) and ions (from the plasma or an independent ion source, typically \( \text{Ar}^+, \text{N}_2^+, \text{N}^+ \)), whose relative fraction depends on the plasma composition and discharge type (MS vs. HiPIMS) \([442,492]\). The film-forming species are either neutral, i.e. sputtered \( \text{Ti}^0 \) atoms from the target, or ionized metallic or nitrogen species, \( \text{Ti}^+, \text{Ti}^{2+}, \text{N}^+ \). The average energy per deposited metallic atoms can be expressed as

\[
E_{\text{d,at}} = E_{\text{d,sp}} + E_{\text{i,Me}} \times J_{\text{Me}} + E_{\text{i,N}} \times J_{\text{N}} + \sum_{i=1}^{n} E_{\text{i,M}} \times J_{\text{i,M}} + E_{\text{i,N}} \times J_{\text{i,N}},
\]

where \( E_{\text{d,sp}} \) is the average energy of sputtered metal atoms, \( J_{\text{Me}} \) is the ion-to-metal flux ratio, \( E_i \) is the average ion energy, \( E_{\text{i,M}} \) is the average energy of backscattered gas species, and \( J_b \) is the flux of backscattered atoms.
The energy of sputtered Ti atoms and reflected Ar depends on the working pressure \( P_{\text{tot}} \) during deposition: these particles will experience collision in the gas phase during their transport from the target to the film surface. For target-to-substrate distance \( d_{\text{TS}} \) lower than the particle mean free path \( \lambda \) (\( \lambda \) is inversely proportional to \( P_{\text{tot}} \)), the particles will reach the substrate with the same nascent energy they had when leaving the target. However, operating at increasing \( P_{\text{tot}} \) can result in \( \lambda \) becoming significantly shorter than \( d_{\text{TS}} \) and particles can get thermalized before reaching the substrate. For example, for Ti atoms, \( \lambda \) decreases from 23 to 9 cm when \( P_{\text{tot}} \) increases from 0.2 to 0.5 Pa [309]. For the same pressure variation, \( E_d \) decreases from 17 eV to 3 eV. The relative flux \( J_{\text{Ar}}/J_{\text{Me}} \) of reflected gas atoms reaching the substrate depends on the metal target mass relative to that of the working gas, as well as and cathode geometry.

For reactive direct current MS (DCMS) in Ar+N\(_2\) plasma discharges, the \( N_2 \) fraction in the sputtering gas mixture is typically several percent and sputtering often occurs under target metal mode. The dominant ion flux reaching the growing film surface is Ar\(^+\), with incident energy \( E_i \) depending on the applied substrate \( V_s \), that is \( E_i = n_i(V_s - V_p) \), where \( V_s \) is the plasma potential (\( \approx 10 \) V) and \( n_i \) the charge state of the ion. The range of \( V_s \), widely used in conventional DCMS deposition of TiN films is 30–60 eV, which is enough to ensure high deposition rates and enhancing adatom surface mobility but may also cause defect incorporation. Operating at higher \( V_s \) (\( > 100 \) eV) will cause film re-sputtering (and consequently roughening) and entrapment of gas atoms (Ar) in the film. The fraction of Ar impurity in TiN films may in this case reach several atomic percent, at the origin of lattice expansion and compressive stresses, as reported by Petrov et al. [493].

Let us summarize the influence of main deposition parameters on the resulting stress state. Increasing \( P_{\text{tot}} \) will result to a net tensile stress increase [487]: increasing N/Ti flux will result to a net compressive stress increase, as seen in Fig. 4a for TiN films deposited at different \( N_2 \) flow, from 6 to 18 sccm, corresponding to N/Ti flux increase from 1 to 23 [487]. Changing the magnetron configuration or operating under rf discharges instead of dc will affect \( J_{\text{Ar}}/J_{\text{Ar}} \) (e.g., \( J_{\text{Ar}}/J_{\text{Me}} \) will increase when unbalancing the magnetron, leading to more compressive stress). The influence of substrate temperature is more complex, as opposing effects can come into play. Increasing \( T_s \) will enhance surface diffusion, promoting incorporation of excess atoms at the grain boundary (compressive stress source), but also activating migration of defects and their annihilation at the film surface (stress relaxation). It can also favor grain growth (tensile stress source) and change in preferential orientation of grains (inducing a stress change for anisotropic elastic material).

The change of texture from [001] to [111] with increasing TiN film thickness (texture crossover) has initially been ascribed to an overall energy minimization, based on thermodynamics considerations that the stored elastic strain energy is lower for [111] planes compared to [002] planes for the same stress level due to elastic anisotropy of TiN crystals. However, there is a converging set of experimental and theoretical findings [268,276,281,282,484,494] which demonstrates that the texture crossover is driven by kinetic limitations intrinsic to the out-of-equilibrium nature of PVD processes, more precisely to anisotropy in surface diffusion.

2.1.2.3. Influence of chemical element and point defects. We briefly review here the variations in stress state of binary TMN, the case of chemical alloying for ternary TMN will be addressed below. The comparative evolution of the intrinsic stress during sputter-deposition of TiN, ZrN and TaN is shown in Fig. 4c, for exactly the same deposition conditions (\( P_{\text{tot}} = 0.3 \) Pa, \( V_s = 50 \) eV) and chamber geometry. One can see that for heavier metal targets (\( M_{\text{Ta}} > M_{\text{Zr}} > M_{\text{Ti}} \)) the stress becomes more compressive, evolving from slightly tensile for TiN towards – 5 GPa for TaN. For TaN, the stress rapidly reaches a steady-state, indicating that there is no significant microstructural change with increasing film thickness. This is related to a loss of columnar structure due to repeated nucleation, TaN films exhibiting a fine grained morphology. These differences can be explained by the contribution of backscattered gas (here Ar) neutrals, whose relative flux and energy increases with Me\(_{\text{tot}}\) [495]. In particular, the average energy of backscattered Ar increases from \( \approx 5 \) eV to \( \approx 57 \) eV when changing Ti to Ta target. \( J_{\text{Me}}/J_{\text{Me}} \) is 0 for a lighter metal target (like Al), \( \approx 3\% \) for Ti target and around 30\% for a heavier metal target (like Ta). The average energy of sputtered atoms also increases from \( \approx 14 \) eV for Ti to \( \approx 25 \) eV for Ta. Both sputtered metal atoms and reflected Ar will contribute to increase \( E_d \) and finally larger compressive stresses will develop as a consequence of defect creation by atomic peening. Changing to a heavier gas atom, like Xe, can be a suitable route to minimize the impact of energetic reflected atoms and reduce the level of compressive stress.

For TiN, Kamminga et al. [496] have shown that atomic peening induces incorporation of misfitting atoms in the TiN layer, causing an hydrostatic state of stress around the defects, and a net compression in the film plane. These authors concluded that, approx. 1\% of Ti atoms on N sites can cause a compressive stress of around \( \approx 5 \) GPa, while the contribution of Ar on N sites will result in lower compressive stress magnitudes (\( \approx 2.2 \) GPa for 1 at.\%). As discussed above, grain boundaries play an important role on the resulting stress state. By varying \( P_{\text{tot}} \) during ZrN sputter-deposition, Koutskerases and Abadias [310] evidenced that at low Ar pressure excess atoms can get trapped in the grain boundary, causing a compressive stress contribution to the total stress state, while at higher Ar pressure, the column/grain boundary are under-dense and the stress due to grain boundary contribution is tensile. If, for the vast majority of cases, the presence of defects in the TMN films is detrimental for their physical properties, they usually contribute to render the material harder. For some TMN, such as MoN and TaN, the existence of point-defects (mainly metal vacancies) is beneficial in stabilizing the cubic structure, as reported recently by Koutna et al. using \textit{ab initio} calculations [387].

2.1.2.4. Consideration for ternary nitrides: stress and microstructure evolution. For many applications, tailoring the physical properties through chemical alloying has become an important research strategy, together with interfacial design. Fig. 5 summarizes the microstructure and stress evolution for two ternary systems, namely Ti-Zr-N and Ti-Ta-N, as representative archetypes of isostructural and non-isostructural pseudo-binary systems, respectively. It can be clearly seen that the degree of [002] texture, \( T_{[002]} \), grain size \( D_- \), microstrain \( \epsilon \) and stress magnitudes are correlated with the variations in \( E_d \) when changing the whole composition range. By increasing the Zr or Ta content in Ti-Zr-N or Ti-Ta-N thin film alloys deposited by reactive DCMS, one can see that the film’s microstructure evolves from [111]-oriented columns towards more fine-grained morphology with [002]-preferred orientation, while the stress becomes more compressive. If cubic Ti\(_1\)-Zr\(_x\)N\(_y\) solid solutions are obtained in the entire compositional range for the Ti-Zr-N system [497], this is no longer the case for the Ti-Ta-N system, as hexagonal phases form above a TaN fraction of \( y \approx 0.7 \). Above this elemental threshold, the value of \( E_d \) becomes relatively large, above 35 eV/at., and it is believed that the large \( \epsilon \) values \( > 1\% \) are responsible for the destabilization of the cubic structure for Ta-rich ternary alloys. A similar behavior was observed for DCMS-deposited Ta-Zr-N alloy thin films [498].

By employing different deposition processes, namely MS, IBS and PLD, Koutskerases et al. [384] have shown that texture evolution of ternary TiTaN as well as the microstructural features of such films can be well understood in the framework of the kinetic
mechanisms proposed for their binary counterparts, thus giving these mechanisms a global application. It was concluded that texture and microstructure are determined by the energetic and kinetic conditions rather by the composition of the film itself. Another system of practical interest is Ti-Al-N. The cubic phase is usually retained up to AlN fractions of 0.6–0.7 depending on the deposition process, while alloys with richer AlN content stabilize in the wurtzite phase. The texture development is influenced by the Al content and deposition rate, but also by the film thickness 

![Graph](image)

**Fig. 5.** Comparative evolution of (a) preferred orientation (T_{002} ratio), b) vertical grain size (D), c) microstrain (ε), d) average stress (σ_{avg}) and e) deposited energy (E_{dep}) for Ti_{1-x}Zr_{x}N (left) and Ti_{1-y}Ta_{y}N (right) systems. The vertical dashed line marks the stability limit of the cubic Ti_{1-y}Ta_{y}N lattice upon Ta incorporation. The arrows indicate the T_{002} ratio for binary powder compounds. The evolution of the microstructure with increasing x (or y) fraction is schematically shown at the bottom in terms of SZM, from Refs. [492,495].
2.2. Optical and electronic properties of continuous films

2.2.1. The work function of B1 transition metal nitrides

The work function WF [184], which dictates the Ohmic or Schottky character of conductor/semiconductor junctions, as well as the potential for hot electron emission, is of particular importance for a variety of applications [110,502–504]. In particular, the height of the Schottky barrier between a conductor and an n-type semiconductor is defined by the conductor’s work function and the semiconductor’s electron affinity [505], as it is presented in Fig. 6a. Thus, for an ideal Ohmic contact on an n-type semiconductor the metal’s WF should be equal to the electron affinity of the semiconductor [505], while a tailored Schottky barrier that would fit certain hot electron applications [110,502–504] could be designed accordingly.

TMN exhibit a quite wide range of WF values, as shown in Fig. 6b. In particular, TMN exhibit WF values in the range of 3.56–5 eV [184,506–508] that coincides with the range of electron affinity values for most elemental and compound semiconductors (yellow shade region) with the major exception of Al-based compound semiconductors (pure AlN, AlP, AlAs). Therefore, by appropriate selection of the nitride conductor and the semiconductor, predesigned Schottky barriers or completely Ohmic contacts can be developed. In addition, good lattice match can be achieved in nitride conductors/nitride semiconductors that may enable epitaxial growth of such heterojunctions [224]. We note here that for simplicity the lattice constants of III-nitrides and their higher melting points compared to the IVb metals? In Fig. 7a with data from Refs. [509–513], and their improved thermal stability (e.g. pure titanium is transformed to anatase at 275 °C [514], while B1-TiN can endure up to 800 °C and is transformed directly to rutile [442]), their most important asset for the applications in photonics and plasmonics is their resemblance to an ideal optical conductor, in contrast to their metallic counterparts. The DC conductivity of transition metals is comparable or lower than that of the corresponding nitrides, as shown in Fig. 7b (with data from Ref. [311,366,432,515–517]), yet their optical behavior is inferior in terms of their plasmonic potential. Therefore, basic questions are risen, such as, what is the difference between an optical conductor and an electrical conductor, and what makes the transition metal nitrides in the B1 cubic structure better optical conductors than the corresponding metals?

In real conductors the measured optical performance is not dictated exclusively by the conduction electrons, in contrast to their DC and AC conductivity, as in the case of ideal conductors often described in textbooks. The real permittivity is screened by the existence of interband transitions of bound electrons. A good optical conductor, which is intended to be used in near-infrared, visible and ultraviolet ranges, should exhibit negative real permittivity (real part of the dielectric function $\epsilon_r$) with a clear and steep crossing to positive values at the wavelength region where the optimal plasmonic performance is desired to be, while its imaginary permittivity (imaginary part of the dielectric function $\epsilon_i$) should have the smallest possible positive values in the entire spectrum, in order to minimize optical losses. A secondary concern is the actual slope of the $\epsilon_r$ at the crossing point ($\epsilon_r = 0$) and the absolute negative values of the conductor; Controlling the absolute negative values of $\epsilon_i$ is highly desirable for several applications [518,519]. An exceptionally comprehensive discussion on this issue can be found in Ref. [135].

In Fig. 8 the real and imaginary permittivities of the group Vb metals (right panels) and their nitrides (left panels) are shown (data from Refs. [380,381,390,520–522]). VN and NbN are undoubtedly better optical conductors than V and Nb, despite of the nitrides having higher DC resistivity according to Fig. 7b, while TaN has a way shorter crossing wavelength than Ta, suggesting a
plasmonic operation at a different spectral range. This contrasting behavior is, indeed, due to the co-existence of intraband (due to conduction electrons) and interband (due to bound electrons) absorption that may, or may not, spectrally overlap; any metal with small DC and AC resistivity may not necessarily be a good optical conductor due to this overlap that occurs exclusively in the range of optical frequencies. When there is strong spectral overlapping (e.g. the case of gold) the dielectric function is screened and the $\varepsilon_1$ gets negative values only for long wavelengths; on the contrary, when the interband and intraband absorption are not overlapping (i.e. if the valence electrons are strongly bound and having energy quite deep compared to the Fermi level, e.g. the case of silver), the conduction electrons are interacting with the light without such screening and the range of negative $\varepsilon_1$ values extents to shorter wavelengths.

The interplay between the intraband and interband absorption and its consequences to the optical spectra, are clearly illustrated in Fig. 9 for the Ti-N system (data from Refs. [176,259,523–526]; note that the $\varepsilon_2$ spectrum of $\varepsilon_1$ close to the Fermi level; finally, for Ti$_3$N$_4$ (i.e. Ti$_{1.12}$) the Ti3d states close to the Fermi level are completely depleted and Ti$_{1.12}$N$_4$ is predicted to be a semiconductor [259].

In order to have a more clear view of the effect of the overlapping of interband and intraband transitions, we show the experimental dielectric function spectra of an opaque B1-TiN film (Fig. 10, red solid lines), which may be analyzed to contributions due to intraband (magenta line) and interband absorption (red dotted line), which were calculated following the procedures described in Ref. [176]; the collective interband absorption (which consists of two Lorentzians) has a maximum at 5.3 eV. Then we calculated two hypothetical nitrides with exactly the same interband and intraband absorption increases (i.e. the interband absorption occurs at lower photon energy) the $\varepsilon_1$ spectra cross the zero line with a less steep slope (if any at all), resembling the optical behavior of Ti and Ti$_2$N in Fig. 9a, and the $\varepsilon_2$ spectra exhibit higher values in the visible range, indicating also higher optical losses. This unequivocally demonstrates the optimal optical behavior of B1-TiN compared to metallic Ti and to all the other phases of the Ti-N system, and we can safely anticipate that this is the origin of the excellent optical behavior of most of the B1 nitrides compared to their metallic counterparts.

2.2.3. Electronic structure calculations

2.2.3.1. Binary nitrides. The origin of electronic conductivity and the spectral position of the interband transitions are closely associated with the bonding configuration of the valence electrons of the constituent metal and nitrogen atoms. Therefore, detailed band structure calculations can shed some light on the correlation between chemical bonding and electronic conductivity in TMN, and they can identify all the features in the reported optical spectra of TMN. Consequently, many groups have performed relevant
detailed calculations of the EDOS for most TMN using various methods and computational packages as demonstrated in Table 1 and the references therein. All these computational works create a consensus that the chemical bonding in TMN is based on the hybridization of the nitrogen’s $p$ electrons with the metal’s $d$ electrons and that the electronic conductivity of TMN is due to the excess $d$ electrons of the metal.

As most of the works in the literature are dealing with some or one of the TMN, in this work, the total ground energy, the lattice parameter and the electron density of states (EDOS) of all the nitrides of the transition metals of the groups IVb-Vb-VIb in the B1 structure (except CrN) have been calculated with the linear augmented plane wave (LAPW) method within the density functional theory using the Wien2k software [527], in order to

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**Fig. 8.** The dielectric function spectra of the group Vb metals (right panels) and of their B1 nitrides (left panels); data from Refs. [380,381,390,520–522].

**Fig. 9.** Spectra of the (a) real, and (b) imaginary parts of the dielectric function for metallic hcp-Ti, $\epsilon$-$\text{Ti}_2\text{N}$, B1-$\text{TiN}$, and the hypothetical calculated Ti$_5$N$_4$ (data from Refs. [176,259,523,524]); (c) linear augmented plane wave calculations of EDOS for hcp-Ti and B1-TiN; (d) valence band spectra acquired by photoemission experiments (data from Refs. [525,526]), the vertical line indicates the Fermi level.
energy regions of occupied states for all TMN: a) from around $E_F$, electrons can enlighten the chemical bonding and the optical reflectivity measurements as two distinct absorption bands, which are particularly the fine structure of the EDOS below the experimentally observed interband transitions [177,184]. In the origin of the partial covalent bonding in these materials, and of this is confirmed both computationally (Fig. 12) and experimentally (Refs. [184,200]).

Fig. 13 summarizes the variations of the EDOS at $E_F$ (which determines the conduction electron density), the wavelengths corresponding to the $E_{01}$ interband transition ($\lambda_{01}$), defined previously in Fig. 11, and the cut-off energy ($\lambda_{\text{cut-off}}$). Some general trends can be identified; in particular, with increasing group numbering of the constituent metal there is an increase of the EDOS value at $E_F$, which is associated with the unscreened plasma energy $E_{pu}$, that depends on the concentration of the conduction electrons of the TMN and is defined by the relation [184,200,550]:

$$E_{pu} = \frac{1}{\sqrt{\epsilon_s}}$$

where $N$ is the conduction electron density, $\epsilon_s$ is the electron charge, $\epsilon_s$ is the permittivity of free space and $m^*$ is the electron effective mass, in SI units. Since $E_{pu}$ is directly correlated with the conduction electron density, it can be used to determine the metallic character of the TMN and it has severe effect on the plasmonic performance of TMN, as we will discuss in the following sections. The enhancement of the EDOS values at the Fermi level with the group numbering of the constituent metal is accompanied by substantial blue shift of $\lambda_{01}$ and $\lambda_{\text{cut-off}}$. With the numbering of both the group and period of the constituent metal (Fig. 13). Note that the $E_{01}$ interband transition is the major source of dielectric losses of all TMN and its spectral location is critical for their plasmonic performance. Therefore, the collective effects of enhancement of the EDOS value at $E_F$ and the reduced dielectric losses at visible wavelengths with increasing group numbering shift the optical absorption and the plasmonic activity of TMN towards the UV. These considerations are vividly illustrated in the spectra of the imaginary part of the dielectric function $\epsilon_2$ calculated from the EDOS [529] and presented in Fig. 14 vs. the wavelength of light, which is more suitable than the photon energy for designing photonic and plasmonic devices. For wavelengths below 500 nm (2.48 eV) the $\epsilon_2$ spectra are dominated by the interband absorption due to bound electrons (Fig. 14a), and the optical absorption is mostly due to the $N-p \rightarrow Metal-d$ interband transition in all cases, while at longer wavelengths (Fig. 14b) the spectra are dominated by the intraband absorption of conduction electrons. Special care should be taken, when we compare computational and experimental $\epsilon_2$ spectra. The computed $\epsilon_2$ spectra correspond to perfect single-crystals at 0 K and, therefore, take into account only the electron-electron scattering and neglect all the other scattering mechanisms, such as scattering of electrons by phonons, point defects and surfaces (grain boundaries) that do contribute to the experimental spectra of polycrystalline films. For these reasons, all the features in the computed $\epsilon_2$ spectra are exceptionally sharp and there is a clear discrimination between the contributions of the
| Reference | Material | Method | Functional | Code | Quantity Calculated | Property Application |
|-----------|----------|--------|------------|------|---------------------|---------------------|
| 1 | [361] | VN, NbN, TaN, CrN, MoN, WN | SAPW | LDA | N/A | EDOS, lattice constant | Carrier density, electron-ion interaction constant, electron-phonon coupling |
| 2 | [473] | TiN, VN, CrN | FLAPW | LDA | N/A | EDOS, lattice constant | Bulk modulus, cube energy, Energy gaps |
| 3 | [485] | TiN | LAPW | GGA (PBE) and LDA | WIEN2k | EDOS, lattice constant | Elastic constants, Bulk modulus, Electronic properties, Elastic constants |
| 4 | [486] | ZrN, NbN | LAPW | LDA | N/A | EDOS, lattice constant | Elastic constants, Bulk modulus, Bulk modulus, Energy gaps |
| 5 | [488] | ZrN, NbN, MoN | LAPW | GGA (PBE) | CASTEP | EDOS, lattice constant | Elastic constants, Bulk modulus, Bulk modulus |
| 6 | [490] | TiN, ZnN | LAPW | GGA (PBE) | VASP | EDOS, lattice constant | Dielectric function, optical reflectivity |
| 7 | [492] | TiN, VN, ZrN, NbN, HfN, TaN | FLAPW | GGA (PBE) and LDA | N/A | EDOS, lattice constant | Cohesive energy, Bulk modulus, Energy gaps |
| 8 | [497] | TiN, ZrN, Ti_xZr_{1-x}N | LAPW | GGA (PBE) | Quantum ESPRESSO | EDOS, lattice constant | Elastic constants |
| 9 | [500] | TiN, VN, CrN | LMTO | LDA | N/A | EDOS, lattice constant | Bulk modulus, Covalent energy |
| 10 | [501] | TiN, VN, CrN | LMTO | LDA | N/A | EDOS, lattice constant | Covalent energy |
| 11 | [502] | TiN, CrN, HfN | LMTO | LDA | N/A | EDOS, lattice constant | Optical reflectivity |
| 12 | [503] | ZrN, NbN, MoN, HfN, TaN | PP | GGA and LDA | CASTEP | EDOS, lattice constant | Elastic constants, Bulk modulus, Elastic constants |
| 13 | [504] | TiN | LAPW | GGA (PBE) | VASP | EDOS, lattice constant | Dielectric function, loss function, optical reflectivity and absorbance |
| 14 | [505] | TiN, VN, CrN, ZrN, NbN | FLAPW | GGA (PBE) and LDA | CASTEP | EDOS, lattice constant | Elastic constants, Bulk modulus, Softness, Electronic and magnetic properties, Elastic constants |
| 15 | [506] | TiN | LAPW | LDA | Quantum ESPRESSO | EDOS, lattice constant | Bulk modulus, Electronic–phonon coupling constant, phonon band structure |
| 16 | [507] | TiN, ZnN, HfN | FLMTO | LDA | N/A | EDOS, lattice constant | Elastic constants, Bulk modulus, Bulk modulus, Debye temperature |
| 17 | [508] | TiN, VN | LAPW | GGA (PBE) and LDA | CASTEP | EDOS, lattice constant | Bulk modulus, Electron–phonon coupling constant, phonon band structure |
| 18 | [509] | TiN, VN, CrN, ZrN, NbN | FLAPW and PP | GGA (PBE) | WIEN2k & SIESTA | EDOS, lattice constant | Elastic constants, Bulk modulus, Bulk modulus, Debye temperature |
| 19 | [510] | TiN | LAPW | LDA | Quantum ESPRESSO | EDOS, lattice constant | Bulk modulus, Electronic–phonon coupling constant, phonon band structure |
| 20 | [511] | TiN | LAPW | LDA | Quantum ESPRESSO | EDOS, lattice constant | Bulk modulus, Electronic–phonon coupling constant, phonon band structure |
| 21 | [512] | TiN, VN, CrN | LMTO | LDA | N/A | EDOS, lattice constant | Elastic constants, Bulk modulus, Bulk modulus, Debye temperature |
| 22 | [513] | TiN, VN, CrN | LMTO | LDA | N/A | EDOS, lattice constant | Elastic constants, Bulk modulus, Bulk modulus, Debye temperature |
| 23 | [514] | TiN, ZnN, HfN | FLAPW and PP | GGA (PBE) | WIEN2k & SIESTA | EDOS, lattice constant | Elastic constants, Bulk modulus, Bulk modulus, Debye temperature |
| 24 | [515] | TiN, VN | LAPW | GGA (PBE) and LDA | VASP | EDOS, lattice constant | Bulk modulus, interband transitions, carrier density, electron-phonon coupling |
| 25 | [516] | TiN, VN, CrN | PWSCF | GGA | N/A | EDOS, lattice constant | Dielectric function spectra |

LAPW: Linearized augmented plane-wave.
FLAPW: Full-potential linearized augmented plane-wave.
PWSCF: Plane-wave self-consistent field.
LMTO: Linear muffin-tin orbital.
FLMTO: Full-potential linear muffin-tin orbital.
IPA: Independent Particle Approximation.
PP: Pseudo-potential.
GGA: Generalized Gradient Approximation.
LDA: Local Density Approximation.
PBE: Perdew–Burke–Ernzerhof, Ref. [528].
PBES: Modified PBE for solids and surfaces, Ref. [543].
PW: Perdew-Wang, Ref. [544].
Quantum ESPRESSO: Ref. [545].
CASTEP: Ref. [546].
ABINIT: Ref. [547].
WIEN2k: Ref. [527].
VASP: Ref. [548].
SIESTA: Ref. [549].
interband transitions (Fig. 14a,c,e) and of the conduction electrons (Fig. 14b,d,f). The computed $\epsilon_2$ spectra at the conduction electron regime (Fig. 14b,d,f) were fitted by the formula of optical dispersion of the Drude theory of metals [550]:

$$\tilde{\epsilon}(\omega) = \epsilon_1 + \epsilon_2 = 1 - \frac{\omega_p^2}{\omega^2 - \Gamma_D \omega},$$

(2)
in order to evaluate the intrinsic electron-electron scattering, which is accountable for the electronic losses, of TMN, through the broadening parameter $\Gamma_D$. $\Gamma_D$ is associated with the conduction electron relaxation time $\tau_D$ [529] as:

$$\Gamma_D(eV) = \frac{\hbar}{\tau_D(s)},$$

(3)
and affects both the material’s resistivity [551]:

$$\rho = \frac{1}{\epsilon_0} \frac{\hbar^2}{\epsilon_{pu}^2} \Gamma_D$$

(4)
and the mean free path $MFP$ of conduction electrons [551]:

$$MFP = \frac{0.75\pi}{(m^*e^2)^{1/3}} \cdot \frac{\hbar^2 \omega_{pu}^3}{\Gamma_D}$$

(5)
Note that the spikes observed in the $\epsilon_2$ spectra in the conduction electron regime (Fig. 14a,c,e) originate from the fine structure of the metal’s $d$-band and can be reasonably neglected as they do not correspond to allowed optical transitions according to the relevant selection rules ($\Delta l = \pm 1$). Fig. 15 shows the variation of intrinsic electron scattering parameter $\Gamma_D$ evaluated from the computed $\epsilon_2$ spectra for the various TMN. The $\Gamma_D$ values are increasing with increasing group number of the constituent metal, due to the observed enhancement of conduction electron density (see also Fig. 12). This is more clearly illustrated in Fig. 16, where the mean free path of conduction electrons (Fig. 16a) and the resistivity (Fig. 16b) of the various B1 nitrides are displayed; these values were determined from Eqs. (4) and (5) by using the $E_{pu}$ and $\Gamma_D$ values extracted from fitting the spectra shown in Fig. 14 and they provide a clear and quantitative view of the inherent electron losses for the perfect single-crystalline materials at 0 K. Indeed, it is evident that group IVb nitrides are the less lossy, with B1-ZrN having the best performance,
while the group Vb nitrides are excessively lossy even in their ideal, defect-free, single-crystalline form; the losses of the latter are further increased by the existence of thermodynamically-favourable point defects [186,387]. Among the group Vb nitrides B1-VN is inferior to B1-NbN and B1-TaN.

Overall, the blueshift of interband transitions of TMN, and consequently of the dielectric losses as well, towards the UV with increasing group number of the constituent metal comes in expense of the intrinsic electronic losses, which are concurrently enhanced. Therefore, this interplay should be taken into account when designing optoelectronic or plasmonic components based on TMN. The combined trends, revealed by analyzing the computed EDOS and ε₂ spectra, clearly demonstrate that the overall decrease of the dielectric losses that originate from the N-Metal bonds via the hybridization of N 2p–Metal d electrons is accompanied by the increase of the density of metal's d states close to the Fermi level, which is expected to result in the increase of electron losses, according to the previous discussion and the data of Fig. 9c,d. The corresponding EDOS of the B1-TixZr1-xN system presented in Ref. [565] shows that the dielectric losses upon incorporation of Zr into TiN (though not as pronounced as for the B1-TixTa1-xN), which is accompanied by reduced density of d electrons close to the Fermi level, and thus resulting in an overall optimal combination of dielectric and electronic losses, while being tunable at the same time. In Ref. [248] the ε₂ spectra of various Ti, Ta, Zr, Nb, Hf, V, N, W, and Mo nitrides have been calculated from the joined density of states (JDOS) determined by LAPW, while the ε₁ spectra were calculated from ε₂ using Kronig integration. The calculated dielectric function spectra are presented in Fig. 18. The optical properties of Ti, Ta, Zr, Nb, Hf, V, N, W, and Mo nitrides with respect to their electronic and dielectric losses, while being tunable at the same time.

Finally, some less studied, emerging systems, such as B1-TixMg1-xN [560], seem particularly interesting. In particular, B1-TixMg1-xN exhibits a semiconductor-conductor transition for x = 0.5 and substantial reduction of conduction electron density for small amounts of Mg; the later is very important for applications in infrared optics and plasmonics [441]. In addition, B1-TixSc1-xN is a stable compound as it has a negative enthalpy of mixing for 0.625 < x < 1 [560]. The competing B1-TixSc1-xN system is stable in the entire compositional range [559], however, for the time being there is no report of a computational study of its optical properties.
these studies two experimental methods of measuring the optical response of the materials were used, namely, spectroscopic ellipsometry (SE), in all of its varieties (variable angle, phase modulated etc), and optical reflectivity spectroscopy (ORS) at near-normal incidence. SE measures the so-called ellipsometric angles \( \Psi / \Delta \). The amplitude ratio \( r_p \) and the phase difference \( \Delta \) between \( p \)- and \( s \)- polarizations are representing the refractive index \( n \) and the extinction coefficient \( k \), respectively. These two ellipsometric parameters are associated with the ratio \( \rho_f \) of the Fresnel reflection coefficients for \( s \)- and \( p \)-polarization through the relationship [569]:

\[
\rho_f = \tan \Psi \cdot e^{i \Delta} = \frac{r_p}{r_s}.
\]  

(6)

Then, the real and imaginary parts of the dielectric function \( \varepsilon = \varepsilon_1 + i \varepsilon_2 \) can by analytically calculated from \( \rho_f \) and the angle of incidence \( \phi \) (usually in the range 55–75°) as [569]:

\[
\varepsilon = \sin^2 \phi \cdot [1 + \tan^2 \phi(\frac{1 - \rho_f^2}{1 + \rho_f})].
\]  

(7)

On the other hand, the real and imaginary parts of the complex refractive index \( n = n + ik \) can be extracted from the spectral reflectivity measurements at normal incidence \( R \) via the relations [570]:

\[
n = \frac{1 - R}{1 + R - 2 \cos \theta \sqrt{R}},
\]  

(8-1)

\[
k = \frac{-2 \sin \theta \sqrt{R}}{1 + R - 2 \cos \theta \sqrt{R}}.
\]  

(8-2)

where \( \theta \) is the phase change due to reflectivity, which is determined by Kramers-Kronig integration [570]:

\[
\theta(\omega) = \frac{1}{\pi} \int_0^\infty \frac{\omega}{\omega_0 - \omega} \frac{d \ln(\sqrt{R(\omega)})}{d \omega} d\omega.
\]  

(9)

Alternatively, the \( n, k \) can be also determined by fitting the spectral reflectivity curves using specific dispersion models [248]. The complex dielectric function and the complex refractive index are equivalent and interchangeable quantities, as they are analytically correlated [571]:

\[
\varepsilon_1 = n^2 - k^2;
\]  

(10-1)

\[
\varepsilon_2 = 2nk.
\]  

(10-2)

In the case of a thin film grown on a bulk substrate the measured spectra by SE or spectral reflectivity accounts the effect of the substrate and film’s thickness, in addition to the film’s optical
properties. Opaque TMN films should be thicker than 100 nm in order to measure directly the complex dielectric function, without any contribution from the substrate; otherwise, a three-phase geometrical model (air/homogeneous film/semi-infinite substrate) \[572\] and knowledge of the substrate’s optical response are required to determine the complex dielectric function of TMN.

In this work, we retrieved and critically review the optical data of TMN from all the references shown in Table 3. We selected these works out of the entirety of the relevant literature because they are reporting directly \(\varepsilon_1, \varepsilon_2\) or \(n, k\) spectra and not just optical reflectivity or transmission values, as the rest of the papers in the literature do. Thus, we can review safely their raw data without any further data handling (e.g., as specified in Eqs. (8) and (9)). Table 3 summarizes the samples grown and the spectra measured by numerous groups worldwide regarding the optical properties of TMN and reviewed in this work. It includes information relevant to the growth conditions, morphology, and the conditions of optical measurements, as well as the corresponding references of Table 3. In order to provide a unified picture and compare all the available data in the literature in a self-consistent manner, we calculated the \(\varepsilon_1, \varepsilon_2\) values using Eq. (9) when the \(n, k\) values are reported in the original references.

The experimental spectra of TMN in most cases are coming from polycrystalline films and they were measured at RT; as a result, the various absorption bands (intraband and interband absorptions) are substantially wider than those of single-crystal materials measured at cryogenic temperatures (which would be directly comparable with the calculated spectra presented in Figs. 14 and 18) and, thus they are overlapping each other. Consequently, it is not possible to spectrally discriminate the intraband and interband absorptions, as we did for the case of the LAPW computational spectra, and a combined Drude-Lorentz model is required for the analysis of the dielectric function spectra \[176\]:

\[
\varepsilon'(\omega) = \varepsilon_\infty - \frac{\alpha_0^2}{\omega^2 - \omega_0^2 - \omega_1^2} + \sum_{j=1}^{2} \left[ \frac{f_j \omega_0^2}{\omega_0^2 - \omega_j^2 - \Omega_j^2 \omega^2} \right],
\]

In Eq. (11) \(\varepsilon_\infty\) is a background constant, larger than unity, which accounts the high-energy contributions (beyond the experimental spectral range) due to transitions that are not taken into account by the Lorentz term(s). Each of the Lorentz oscillators \((n = 1 \text{ or } 2)\) is located at an energy position \(E_j = \hbar \omega_0\) with strength \(f_j\) and damping (broadening) factor \(\Gamma_j\). The Drude term is characterized by the unscreened plasma energy \(E_\text{pu} = \hbar \omega_0\) and the damping factor \(\Gamma_\text{D}\) as mentioned previously. All the \(\varepsilon_1, \varepsilon_2\) spectra retrieved from the works summarized in Table 3 were fitted by a least-square regression algorithm using Eq. (11) with mostly two Lorentz oscillators \((n = 2)\) within the Horiba Jobin-Yvon Delta-Psi\textsuperscript{16} software. The use of two Lorentz oscillators physically describes the absorption bands \(E_01\) and \(E_02\) as identified by the LAPW data in Fig. 11. In the cases where the second Lorentz oscillator was far beyond the experimental spectral range, or the fitting process had substantial uncertainties (by means of the least square values when using two oscillators \((n = 2)\), or the fitting rendered values without a physical meaning for the second oscillator (e.g., coinciding spectral energy of the two oscillators, strength or broadening parameters close to zero, etc.) we utilized Eq. (11) with only one Lorentz oscillator \((n = 1)\). In the rare cases of spectra corresponding to non-opaque \((\text{thickness } < 100 \text{ nm})\) films, the least-square regression fit was combining Eq. (11) with a three-phase geometrical model \((\text{air/film/substrate})\) \[573\]; note that for these cases, we did not have accurate knowledge of the \(\varepsilon_1, \varepsilon_2\) spectra of the substrates, and therefore, our corresponding fitting might be of questionable accuracy. Finally, we did not manage to fit adequately the data presented in Ref. \[285\], so in the following text wherever Ref. \[285\] is mentioned, its raw data are used, albeit without too much compromise, since the thickness of the films reported where above 100 nm and so any contribution from the substrate would be negligible.

The quantitative results of the fits are summarized in Table 4. Representative experimental spectra from various opaque TMN films from Refs. \[197,303,380\] along with the corresponding fit results and the deconvolutions to the individual contributions of the Drude term \((\text{intraband absorption})\) and the two Lorentz terms \((\text{interband absorptions } E_01\text{ and } E_02)\) are presented in Fig. 19 (note that the wavelength of the \(x\)-axis is in reciprocal scale to resemble the variation of photon energy). Based on the excellent fit quality in most cases, we extrapolated the \(\varepsilon_1, \varepsilon_2\) spectra using the values of the parameters of the best fit listed in Table 4 in the spectral range 200–1300 nm as presented in Fig. 19, in order all the spectra to be comparable to each other. The extrapolated spectra of the real and imaginary parts of the dielectric function \((\text{or equivalently of the real and imaginary permittivity})\) for all the studied samples listed in Table 3 are presented in Figs. 20 and 21, respectively.

In particular for Fig. 20, the typical metallic and featureless lineshape of negative \(\varepsilon_1\) for long wavelengths (>450 nm) is observed only for group IVb nitrides (TiN, ZrN, HfN) and VN. This spectral region is characterized by negative values of \(\varepsilon_1\) due to the interaction of light with the conduction electrons of the corresponding nitrides, i.e. due to intraband absorption.

Among the group IVb nitrides (TiN, ZrN, HfN), TiN is the most widely studied so far and exhibits the wider range of absolute values of \(\varepsilon_1\) vs. the wavelength compared to the most well-reproducible ZrN; HfN exhibits an intermediate scattering of \(\varepsilon_1\) values. The absolute values of \(\varepsilon_1\) at long wavelengths are affected by both the electron density and the electron losses, and thus...
indirectly by the film’s composition and stoichiometry, respectively. The scattering of the $\varepsilon_1$ experimental values reported by various groups using various growth techniques indicate that TiN is the nitride with the highest tailoring potential (possibly due to its ability to accommodate excess nitrogen and form over-stoichiometric films [176], as well as the large variety of microstructural features observed in TiN films as we have previously shown in Section 2.1.2), while ZrN is best in terms of stability and reproducibility of its optical performance.

NbN and MoN exhibit also negative $\varepsilon_1$ values for long wavelengths, but lower absolute values than what is observed for TiN, ZrN, HfN, and VN. This is due to high values of electronic losses (characterized by higher values of the $G_D$ parameter), which are an inherent characteristic of NbN and MoN, as mentioned previously when discussing Figs. 15 and 16, and further enhanced by the poor crystalline quality of the corresponding studied MoN samples. Finally, TaN and WN are more complicated cases, as most of their spectra do not exhibit the simplified metallic lineshape. For TaN, this is due to the coexistence of two or more crystal phases (i.e. the films do not consist exclusively of the B1 phase as stated in the comments of Table 3), the existence of high density of point defects in TaN [387] and the ultrafine grain sizes, as presented in Fig. 5, which further increase the scattering of electrons and the relevant electronic losses beyond the level of the rest of the studied nitrides. These inherent drawbacks of B1-TaN can be overcome by alloying with a small concentration of Ti to form B1-Ti$_x$Ta$_{1-x}$N, as we will discuss later in more detail. Finally, the WN are so lossy, due to the excessive incorporation of point defects [432,574], so as their $\varepsilon_1$ do not have negative values in the visible and near infrared ranges at all. In fact, the high electron losses of B1-WN cause the $\varepsilon_1$ to remain positive up to very long wavelengths in the infrared region, becoming negative only above

Table 2
A review of the computational studies of EDOS of various ternary TMN.

| Reference | Material                  | Method  | Functional | Code      | Quantity Calculated Property-Application |
|-----------|---------------------------|---------|------------|-----------|-----------------------------------------|
| 7 [248]   | Ti$_x$Ta$_{1-x}$N         | LAPW    | GGA (PBE)  | Wien2k    | EDOS, lattice constant                   |
| 6 [249]   | Ti$_x$Ta$_{1-x}$N, Ti$_x$Zr$_{1-x}$N | LAPW    | GGA (PBE)  | Wien2k    | EDOS, lattice constant                   |
| 11 [252]  | Ti$_x$Ta$_{1-x}$N         | LAPW    | GGA (PBE)  | ABINIT    | EDOS, lattice constant                   |
| 14 [498]  | Ta$_x$Zr$_{1-x}$N         | LAPW    | GGA (PBE)  | VASP      | EDOS, lattice constant                   |
| 9 [535]   | Ti$_x$V$_{1-x}$N, Ti$_x$Nb$_{1-x}$N, Ti$_x$Ti$_{1-x}$N, Ti$_x$W$_{1-x}$N, V$_x$Nb$_{1-x}$N, V$_x$Ta$_{1-x}$N, V$_x$W$_{1-x}$N | PWG     | GGA (PW)   | VASP      | EDOS, lattice constant                   |
| 1 [552]   | Ti$_x$Al$_{1-x}$N         | PAW     | GGA        | VASP      | EDOS, lattice constant                   |
| 2 [553]   | Ta$_x$Zr$_{1-x}$N         | PP      | GGA (PW)   | CASTEP    | EDOS, lattice constant                   |
| 3 [554]   | Ti$_x$Al$_{1-x}$N         | PAW     | GGA        | VASP      | EDOS, lattice constant                   |
| 4 [555]   | Ti$_x$Al$_{1-x}$N, Hf$_x$Al$_{1-x}$N | PAW     | GGA        | VASP      | EDOS, lattice constant                   |
| 5 [556]   | Ti$_x$Zr$_{1-x}$N, Ti$_x$Al$_{1-x}$N | FLMTO   | HL         | N/A       | Mixing enthalpy                          |
| 8 [557]   | Ti$_x$Mo$_{1-x}$N, Ti$_x$W$_{1-x}$N | PAW     | GGA (PW)   | VASP      | EDOS, lattice constant                   |
| 10 [558]  | Ti$_x$Zr$_{1-x}$N         | PAW     | GGA (PW)   | ABINIT    | Bulk modulus, elastic constants          |
| 12 [559]  | Ti$_x$Sc$_{1-x}$N, Zr$_x$Sc$_{1-x}$N, Hf$_x$Sc$_{1-x}$N, V$_x$Sc$_{1-x}$N, Nb$_x$Sc$_{1-x}$N, Ta$_x$Sc$_{1-x}$N | PAW     | GGA (PBE)  | VASP      | Mixing enthalpy                          |
| 13 [560]  | Ti$_x$Mg$_{1-x}$N         | PAW     | GGA        | VASP      | EDOS, lattice constant                   |
| 15 [611]  | Ti$_x$Mo$_{1-x}$N, Ta$_x$W$_{1-x}$N | LAPW    | GGA (PBE)  | ABINIT    | EDOS, lattice constant                   |
| 16 [562]  | Ti$_x$V$_{1-x}$N, Ti$_x$Zr$_{1-x}$N, Ti$_x$Hf$_{1-x}$N, Ti$_x$Nb$_{1-x}$N, Ti$_x$Ta$_{1-x}$N | PAW     | GGA (PBE)  | VASP      | Bulk modulus, deformation                |
| 17 [563]  | Ti$_x$W$_{1-x}$N         | PAW     | GGA (PW)   | VASP      | Bulk modulus, deformation                |
| 18 [564]  | Ta$_x$Hf$_{1-x}$N         | N/A      | N/A        | N/A       | EDOS                                    |
| 19 [565]  | Ti$_x$Zr$_{1-x}$N         | PAW     | GGA (PBE)  | VASP      | Dielectric function spectra, reflectivity, loss function, plasmonic field enhancement |
| 20 [566]  | V$_x$Al$_{1-x}$N         | PAW     | GGA (PBE)  | VASP      | EDOS                                    |
| 21 [567]  | Ti$_x$Zr$_{1-x}$N, Ti$_x$Hf$_{1-x}$N, Zr$_x$Hf$_{1-x}$N | PAW     | GGA (PBE)  | VASP      | EDOS, lattice constant                   |

LAPW: Linearized augmented plane-wave.
PAW: Projected Augmented Wave.
FLMTO: Full-potential linear muffin-tin orbital.
PP: Pseudo-potential.
GGA: Generalized Gradient Approximation.
PBE: Perdew–Burke–Ernzerhof, Ref. [528].
PW: Perdew-Wang, Ref. [544].
HL: Hedin-Lundqvist, Ref. [568].
CASTEP: Ref. [546].
ABINIT: Ref. [547].
WIEN2k: Ref. [527].
VASP: Ref. [548].

Fig. 17. EDOS of the B1-Ti$_x$Ta$_{1-x}$N system calculated by LAPW in Ref. [248]. The composition x affects both the conduction $d$ electron density (vertical arrow) and the range of the dielectric losses (diagonal arrow).
22 μm [432]. This challenges the perspectives of B1-WN for applications in mainstream plasmonics contrary to what has recently been proposed [542]. On the contrary, WN may be promising as high electron loss was recently highlighted as a pathway for implementing localized plasmon-enhanced photothermal processes such as photothermal therapy [575], and as a potential tunable epsilon-near-zero (ENZ) material [576] due to the varying moderate slope of the ε1 spectrum vs. photon wavelength that results in wide wavelength regions where ε1 is nearly zero.

Of particular importance is the energy that corresponds to the wavelength of light where ε1 = 0. This energy is defined as the screened plasma energy $E_{ps} = \frac{\hbar \omega_{ps}}{\epsilon_0 c} \sqrt{\frac{N_{eff}}{m}}$, and is affected by both the intraband and interband characteristics. In the case of the non-existent ideal conductor where there are no bound electrons $E_{ps} = E_{pu}$. As an example, $E_{pu}$ and $E_{ps}$ for NbN are indicated by vertical arrows in Fig. 19b and their physical interpretations are clearly distinguished. $E_{ps}$ and/or $\lambda_{ps}$ separate the dielectric function spectra into two regions; the one is for long wavelengths ($\lambda > \lambda_{ps}$) where the light is reflected by the conductor due to conduction electrons, and the other is for short wavelengths ($\lambda < \lambda_{ps}$) where the conductor is semitransparent and exhibits moderate light attenuation exclusively due to interband absorption. When $\lambda_{ps}$ lies into the visible spectral range, it actually defines the color of the conductor, as it is shown for representative nitrides in Fig. 22; thus $\lambda_{ps}$ defines the reflectivity edge. When $\lambda_{ps}$ lies into the visible range, then it also defines the color of the conductor. $E_{ps}$ and/or $\lambda_{ps}$ was also introduced as an indicator of the stoichiometry of TiN ($E_{ps}$ gets the value 2.65 eV for $x = 1$ [572]); consequently, the actual visual appearance and the color is a safe indicator for TiN and other TMN. Thus, high-quality stoichiometric TiN is bright yellow, overstoichiometric lossy TiN is reddish brown, ZrN and HfN are pale yellow, NbN is greenish extra-pale yellow, and TaN in the B1 structure is dim grey (dim due to the high electron loss resulting in low reflectivity as it is shown in Fig. 22, and grey because its $\lambda_{ps}$ is at the verge of the visible range, thus reflecting the entire visible spectrum). A wider color palette can be achieved by ternary nitrides [471].

Although $E_{ps}$ does not have any clear physical meaning other than that $\epsilon_1 = 0$ for real conductors, it was found to indicate, but not to coincide with, the spectral position of SPP and LSPR in TiN [177] and in ternary nitride nanostructures [439,441], and therefore, it has major practical importance for plasmonics.

Below $E_{ps}$ (i.e. for longer wavelengths) the negative values of $\epsilon_1$, in combination with positive values of $\epsilon_2$, imply that the light propagation is not allowed through the conductor and the corresponding skin depth is infinitesimal small. Beyond $E_{ps}$ (i.e. for shorter wavelengths) positive values of $\epsilon_1$ are observed, which are associated with the interband absorption and the dielectric losses. In this range the nitride conductors are semitransparent to light, which can pass through them with a moderate attenuation due to the dielectric losses. The interband transitions can be more clearly seen in Fig. 21, where we present the extrapolated $\epsilon_2$ values for all binary nitrides, and $\lambda_{ps}$ is also indicated by the diagonal arrow in Fig. 21a for the case of TiN. The scaling of $\epsilon_2$ values in the y-axis is the same in all graphs, in order to make them comparable. The corresponding dielectric losses are minimized for ZrN and NbN among the nitrides of IVb and Vb group elements, respectively, suggesting these nitrides as the most promising in terms of the lack of contribution of dielectric losses in their optical spectra and plasmonic properties. From the structural point of view, which affects mostly the electron losses [176], the growth of ZrN is usually accompanied by a substantial amount of structural defects [441,471]. Indeed, sputtered ZrN films deposited at the same growth conditions (pressure, substrate bias and target power) with TiN, exhibited substantially higher compressive intrinsic stress [309] due to the backscattered Ar$^+$ ions from the Zr target, the reduced thermalization of Zr atoms in the gas phase and the reduced mobility of Zr adatoms on the active growing surface [309,310], all of them due to the higher atomic mass of Zr compared to Ti as also presented in Section 2.1.2.3 of this work; for all these reasons the growth of pure epitaxial ZrN films was achieved quite recently [311], despite of the growth of ZrN films, which include some epitaxial domains since the late eighties [312]. On the contrary, the epitaxial growth of NbN is quite usual on various substrates [581–584].

Coming back to $E_{ps}$, and in an effort to predict the spectral range of plasmonic effects in TMN, it is important to investigate the potential correlation of it with the effective number of valence electrons $N_{eff}$ of the constituent metals (4, 5, 6 for IVb, Vb, VIb metals, respectively) of conductive nitrides. Fig. 23 displays this correlation. Despite of the wide scattering of experimental points, there is an identifiable trend of increasing the $E_{ps}$ on the average when $N_{eff}$ increases from 4 (TiN, ZrN, HfN) to 5 (VN, NbN, TaN) suggesting that VN, NbN and TaN would exhibit blueshifted plasmonic features compared to TiN, ZrN, HfN. This behavior is assigned to the increased conduction electron density of the nitrides of the group Vb metals. On the contrary, the nitrides of the group Vb metals (MoN, WN) exhibit reduced $E_{ps}$ vaues compared to the group Vb nitrides despite their expected increased conduction electron density. This is accompanied by excessive electron losses [184,432], which are responsible for this phenomenological behavior. As a result, an $E_{ps}$ spectral range of 1.99–3.51 eV (equivalent to wavelengths 623–353 nm) can be covered by binary TMN. The spectral range of $E_{ps}$ cannot be used on its own merit as a benchmark for the plasmonic performance of conductive

Fig. 18. Dielectric function spectra for the B1-Ti$_x$Ta$_{1-x}$N system determined from the EDOS calculated by LAPW in Ref. [248]. The insets shows the variation of $E_{ps}$, $\epsilon_{1D}$, $\epsilon_{2D}$ and $\rho$ vs. $x$ determined from the spectra using Eqs. (2), (4), (5).
| No. | Reference | First Author | Growth Technique | Film Material | Substrate | Thickness (nm) | Morphology | Measurement Technique | Instrument | Experimental spectral range (nm) | Comments |
|-----|-----------|--------------|------------------|---------------|-----------|---------------|------------|----------------------|------------|-------------------------------|----------|
| 1   | [286]     | Edlou        | Magnetron Sputtering | TiN, HfN | Fused Silica | Opaque | N/A | VASE | N/A | 240–1660 | Stoichiometry determined by RBS; (100) Oriented identified by XRD; composition determined by RBS and XPS; ORS measurements acquired using an integrating sphere; ORS normalization was performed via a Si(100) wafer. |
| 2   | [240]     | Gall         | UHV Sputtering | TiN | MgO(100) | 200 | Epitaxial | ORS | Perkin Elmer | 413–2400 | Stoichiometry determined by XPS and RBS; crystal structure identified by XRD Used halide precursors; Stoichiometry close to 1 determined by EPMA and by the cubic lattice size (0.424 nm) determined by XRD; no Cl impurities; C impurities <0.2% wt. |
| 3   | [292]     | Huber        | Me-PIII | TiN | Si(100) | 100–500 | Polycrystalline | SE | RAE | 248–826 | Stoichiometry x=0.95 determined by ERDA; crystal structure identified by XRD |
| 4   | [291]     | Humlicek     | IBAD | TiN | Si(100) | 50–100 | Polycrystalline | VASE | RAE | 350–1650 | Stoichiometry determined by XRD and RBS; crystal structure identified by XRD used halide precursors; Stoichiometry close to 1 determined by EPMA and by the cubic lattice size (0.424 nm) determined by XRD; no Cl impurities; C impurities <0.2% wt. |
| 5   | [285]     | Karlsson     | CVD | TiN, ZrN, HfN | Polished Mo | ~1000 | Polycrystalline | ORS | Perkin Elmer | 200–4900 | Stoichiometry close to 1 determined by XRD and RBS; crystal structure identified by XRD used halide precursors; Stoichiometry close to 1 determined by EPMA and by the cubic lattice size (0.424 nm) determined by XRD; no Cl impurities; C impurities <0.2% wt. |
| 6   | [434]     | Koutsokeras  | DIBS | TiN | Si(100) | >300 | Globular polycrystalline | VASE | RPE by SOPRA | 200–1200 | Stoichiometry x=1 determined by AES and XPS; crystal structure identified by XRD Used TiCl₄, H₂, and N₂ precursors; x < 1 The TiN[111]/Al₂O₃[0006] epitaxy was confirmed by XRD Growth at 400 °C and Bias voltage of ~100 V; Stoichiometry close to 1 confirmed by XPS; crystal structure and (100) texture identified by XRD Growth at RT and Bias voltage of ~120 V; Stoichiometry x=1 determined by XPS; crystal structure and (100) texture identified by XRD |
| 7   | [294]     | Langereis    | ALD | TiN | H-terminated Si | >100 | Polycrystalline | in situ SE | RCE by J.A. Woolam | 250–1650 | Stoichiometry close to 1 confirmed by XPS; crystal structure identified by XRD Growth at 400 °C and Bias voltage of ~100 V; Stoichiometry x=1 determined by XPS; crystal structure and (100) texture identified by XRD |
| 8   | [170]     | Naik         | Magnetron Sputtering | TiN | c-Sapphire | 30 | Epitaxial | VASE | RCE by J.A. Woolam | 250–2000 | Stoichiometry close to 1 confirmed by XPS; crystal structure and (111) texture identified by XRD Growth at RT and Bias voltage of ~20 V; Stoichiometry x=1 determined by XPS; crystal structure and (111) texture identified by XRD |
| 9   | [176]     | Patsalas     | Magnetron Sputtering | TiN | Si(100) | >100 | Polycrystalline | in situ SE | PME by JY-Horiba | 225–826 | Stoichiometry close to 1 confirmed by XPS; crystal structure and (100) texture identified by XRD Growth at 400 °C and Bias voltage of ~100 V; Stoichiometry x=1 determined by XPS; crystal structure and (100) texture identified by XRD Growth at RT and Bias voltage of ~120 V; Stoichiometry x=1 determined by XPS; crystal structure and (100) texture identified by XRD |
| 10  | [176]     | Patsalas     | Magnetron Sputtering | TiN | Si(100) | >100 | Polycrystalline | in situ SE | PME by JY-Horiba | 225–826 | Stoichiometry close to 1 confirmed by XPS; crystal structure and (111) texture identified by XRD Growth at RT and Bias voltage of ~20 V; Stoichiometry x=1 determined by XPS; crystal structure and (111) texture identified by XRD |
| 11  | [176]     | Patsalas     | Magnetron Sputtering | TiN | Si(100) | >100 | Columnar Polycrystalline | in situ SE | PME by JY-Horiba | 225–826 | Stoichiometry close to 1 confirmed by XPS; crystal structure and (111) texture identified by XRD Growth at RT and Bias voltage of ~20 V; Stoichiometry x=1 determined by XPS; crystal structure and (111) texture identified by XRD |
| No | Reference | First Author | Growth Technique | Film Material | Substrate | Thickness (nm) | Morphology | Measurement Technique | Instrument | Experimental spectral range (nm) | Comments |
|----|-----------|--------------|------------------|--------------|-----------|---------------|------------|----------------------|------------|-------------------------------|----------|
| 12 | [177]     | Patsalas     | PLD              | TiN          | Si(100)   | >100          | Polycrystalline | VASE        | PME by JY-Horiba            | 191–826   | Growth at RT; Stoichiometry x=1 determined by in situ XPS; crystal structure and (111) texture identified by XRD. Spectral normalization was performed via a Si wafer. TcCl<sub>4</sub> and NH<sub>3</sub> precursors; Overstoichiometry determined by XPS; Existnt Cl-impurities. |
| 13 | [321]     | Postava      | Sputtering      | TiN          | Thick thermal SiO<sub>2</sub> | 107.1 | N/A | ORS | Shimadzu              | 225–826   | Spectral normalization was performed via a Si wafer. Used TiCl<sub>4</sub> and NH<sub>3</sub> precursors; Overstoichiometry determined by XPS; Existnt Cl-impurities. |
| 14 | [295]     | Van Bui      | ALD              | TiN          | 100 nm SiO<sub>2</sub>/Si | 10 | N/A | in situ SE | RCE by J.A. Woolam | 250–1650 | Growth at 600 °C; Stoichiometry determined by ERDA; crystal structure identified by XRD. Stoichiometry equals to 1 confirmed by RBS; Overstoichiometry determined by XPS; Existnt Cl-impurities. |
| 15 | [238]     | Wiemer       | Magnetron Sputtering | TiN          | Si(100)   | 400          | Polycrystalline | SE | PME by JY-Horiba            | 413–826   | Stoichiometry determined by ERDA; crystal structure identified by XRD. Stoichiometry determined by EPMA; a cubic lattice size (0.460 nm) determined by XRD; the chemical and structural data were reported in Ref. [528]. |
| 16 | [244]     | Aouadi       | Magnetron Sputtering | ZrN          | Si(111)   | 1500         | Polycrystalline | VUV-VASE | RAE by J.A. Woolam | 150–600   | Stoichiometry determined by EPMA; Overstoichiometry determined by XPS; Existnt Cl-impurities. |
| 17 | [126]     | Camelio      | Magnetron Sputtering | ZrN          | Si(100)   | 100          | Polycrystalline | VASE | RPE by SOPRA            | 200–1200  | Stoichiometry determined by EPMA; a cubic lattice size (0.460 nm) determined by XRD; the chemical and structural data were reported in Ref. [528]. |
| 18 | [303]     | Mei          | Magnetron Sputtering | ZrN          | MgO(100)  | 830          | Epitaxial    | VASE        | RCE by J.A. Woolam            | 240–1200  | Stoichiometry determined by EPMA; a cubic lattice size (0.460 nm) determined by XRD; the chemical and structural data were reported in Ref. [528]. |
| 19 | [174]     | Naik         | Magnetron Sputtering | ZrN, HfN, TaN | c-Sapphire | 30–50         | N/A | SE | RCE by J.A. Woolam            | 250–2000  | Stoichiometry determined by EPMA; a cubic lattice size (0.462 nm) determined by XRD; the chemical and structural data were reported in Ref. [528]. |
| 20 | [324]     | Pilloud      | Magnetron Sputtering | ZrN          | Stainless steel | 3000         | Polycrystalline | VASE | RPE by SOPRA            | 200–1200  | Stoichiometry determined by EPMA; a cubic lattice size (0.462 nm) determined by XRD; the chemical and structural data were reported in Ref. [528]. |
| 21 | [325]     | Veszelei     | Magnetron Sputtering | ZrN          | SiO<sub>2</sub>/Si | Opaque | N/A | SE | RCE by J.A. Woolam            | 250–2500  | Stoichiometry determined by WDS; the B1 structure identified by XRD. Stoichiometry determined by XPS; the B1 structure identified by EPMA; a cubic lattice size (0.4575 nm) determined by XRD and HRTEM. |
| 22 | [328]     | Gueddoua     | Magnetron Sputtering | HfN          | Si(100)    | 50           | Polycrystalline | ORS | Perkin Elmer             | 250–2500  | Stoichiometry determined by WDS; the B1 structure identified by XRD. Stoichiometry determined by XPS; the B1 structure identified by EPMA; a cubic lattice size (0.4575 nm) determined by XRD and HRTEM. |
| 23 | [577]     | Hu           | Magnetron Sputtering | HfN          | Si(100)    | 614          | Polycrystalline | ORS | Perkin Elmer             | 250–2500  | Stoichiometry determined by WDS; the B1 structure identified by XRD. Stoichiometry determined by XPS; the B1 structure identified by EPMA; a cubic lattice size (0.4575 nm) determined by XRD and HRTEM. |
| 24 | [327]     | Stromme      | Magnetron Sputtering | HfN          | Hf/borosilicate glass | 53           | N/A | ORS | Monolight OSA            | 230–2000  | Stoichiometry determined by WDS; the B1 structure identified by XRD. Stoichiometry determined by XPS; the B1 structure identified by EPMA; a cubic lattice size (0.4575 nm) determined by XRD and HRTEM. |
| 25 | [380]     | Mistriki     | Magnetron Sputtering | VN, TaN      | Fused Silica | 100          | N/A | Null Ellipsometry | N/A | 248–826 | Composition determined by AES; VN is stoichiometric; TaN is understoichiometric and likely includes the Ta<sub>2</sub>N phase. |
| No. | Reference | First Author | Growth Technique | Film Material | Substrate | Thickness (nm) | Morphology | Measurement Technique | Instrument | Experimental spectral range (nm) | Comments |
|-----|-----------|--------------|------------------|---------------|-----------|---------------|------------|----------------------|------------|-------------------------------|----------|
| 26  | [391]     | Konevecki    | Magnetron Sputtering | NbN           | Borosilicate Glass | 110 | Columnar Polycrystalline | SE | RAE | 248–826 | Stoichiometry determined by XPS; XRD identified the B1 phase |
| 27  | [390]     | Sanjines     | Magnetron Sputtering | NbN           | Si wafer | N/A | N/A | SE | PME by JY-Horiba | 250–1650 | Stoichiometry NbN, determined by EPMA and RBS; XRD identified the B1 phase |
| 28  | [389]     | Tanabe       | Magnetron Sputtering | NbN           | SiO₂/Si | 200–300 | Polycrystalline | ORS | N/A | 200–1000 | Stoichiometry NbN, determined by AES; XRD identified the B1 phase |
| 29  | [578]     | Aosaki       | Magnetron Sputtering | TaN           | Si(100) | Opaque | Nanocrystalline | VASE | RCE by J.A. Woolam | 150–600 | Stoichiometry NbN, determined by XPS; XRD identified just one broad peak that may correspond to the (111) of B1-TaN or the (0002) of h-TaN |
| 30  | [579]     | Bousquet     | Magnetron Sputtering | TaN           | Vitreous carbon | N/A | Mixed Phase Polycrystalline | SE | PME by JY-Horiba | 261–1653 | Overstoichiometric mixed phase films studied by RBS and XRD |
| 31  | [382]     | Langereis    | ALD               | TaN           | p-Si wafer | 52 | Polycrystalline | In situ SE | RCE by J.A. Woolam | 250–1650 | Stoichiometry equals to unity determined by RBS; the B1 phase identified by XRD |
| 32  | [381]     | Matenoglou   | PLD               | TaN/(100)     | Si(100) | 300 | Nanocrystalline | VASE | RPE by SOPRA | 200–1200 | Film slightly underdense; Stoichiometry TaN, determined by AES; the B1 structure identified by XRD |
| 33  | [580]     | Waechtler    | Magnetron Sputtering | TaN           | Si wafer | 380 | N/A | SE | RAE by SENTECH | 250–2500 | Stoichiometry B1-TaN and h-TaN phases |
| 34  | [184]     | Matenoglou   | PLD               | MoN, WN       | Si(100) | 300 | Nanocrystalline | ORS | Avantes | 250–780 | Stoichiometry [N]/[Me]=0.98 was determined by AES; B1 phase identified by XRD; experimental spectra restricted to λ > 275 nm |
| 35  | [431]     | Parreira     | Magnetron Sputtering | WN            | Si wafer | N/A | Nanocrystalline | SE | PME by JY-Horiba | 275–826 | Stoichiometry not available; most likely a mixed phase film |
| 36  | [432]     | Metaxa       | UHV Sputtering    | WN            | MgO(111) | 2500 | Epitaxial | ORS | Avantes, OceanOptics, Bruker | 193–100000 | Epitaxial B1-WN(111)/MgO(111) testified by XRD and HRTEM; Stoichiometry [N]/[W]=0.87 was determined by XPS. |

a] SE = Spectroscopic Ellipsometry, VASE = Variable-Angle Spectroscopic Ellipsometry, ORS = Normal-Incidence Optical Reflectivity Spectroscopy, VUV = Vacuum UV.

b] RAE = Rotating Analyzer Ellipsometer, RCE = Rotating Compensator Ellipsometer, RPE = Rotating Polarizer Ellipsometer, PME = Phase-Modulated Ellipsometer.

c] RBS = Rutherford Backscattering, ERDA = Elastic Recoil Detection Analysis, XPS = X-Ray Photoelectron Spectroscopy, AES = Auger Electron Spectroscopy, EPMA = Electron Probe Microanalysis, WDS = Wavelength-Dispersive Spectroscopy, XRD = X-Ray Diffraction, HRTEM = High-Resolution Transmission Electron Microscopy.
TMN; in order a conductor to be a viable candidate for plasmonics, it has to exhibit as low electron loss as possible. Consequently, it is very important to correlate the parameter $\Gamma_D$, which is associated with the electron loss, with $E_{pu}$ or its equivalent wavelength $\lambda_{ps}$ in order to evaluate the expected electron losses at various operational wavelengths for plasmonic devices. Such a correlation is important to correlate the parameter $\Gamma_D$, with the electron loss, with $E_{pu}$ and $\lambda_{ps}$.

Table 4

| Material | Spectra from Ref. | First Author | $\epsilon_{\infty}$ | $E_{pu}$ (eV) | $\Gamma_\text{D}$ (eV) | $f_1$ | $E_1$ (eV) | $\gamma_1$ (eV) | $f_2$ | $E_2$ (eV) | $\gamma_2$ (eV) | $E_{pu}$ (eV) | $\rho$ (\mu\Omega cm) |
|----------|------------------|-------------|-----------------|--------------|----------------------|------|--------------|----------------|------|--------------|----------------|--------------|------------------|
| TiN [286] | Egdou          | 2.35        | 7.25            | 0.64         | 0.23                  | 2.07 | 0.75         | 0.54          | 4.04 | 5.65        | 3.62          | 2.75         | 94               |
| TiN [240] | Gall            | 8.78        | 9.77            | 0.35         | 0.40                  | 2.00 | 0.82         | 4.58          | 8.23 | 4.04        | 2.59          | 29               |
| ZrN [232] | Huber           | 3.00        | 8.08            | 0.86         | 3.54                  | 5.14 | 3.04         | N/A           | N/A  | 2.90        | 102           | N/A             |
| ZrN [251] | Humikek         | 3.84        | 6.42            | 0.86         | 3.12                  | 3.77 | 1.55         | N/A           | N/A  | 2.15        | 161           | N/A             |
| HfN [285] | Karlssoon       | N/A         | N/A             | N/A          | N/A                  | N/A  | N/A          | N/A           | N/A  | N/A         | N/A           | N/A             |
| SiN [434] | Koutsokeras     | 2.13        | 7.03            | 0.63         | 0.38                  | 3.71 | 1.33         | 4.35          | 5.88 | 4.28        | 2.55          | 98               |
| Langeres  | 3.87           | 7.21        | 0.81            | 2.69         | 4.48                  | 2.64 | 1.27         | 5.36          | 0.88 | 2.32        | 120           |                 |
| Naik [170] | 2.67           | 5.71        | 0.17            | 0.20         | 2.26                  | 0.72 | 2.31         | 4.89          | 3.88 | 1.99        | 39            |                 |
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In order to interpret the variations of the conduction electron density, via $E_{pu}$ and Eq. (1), and the conduction electron loss, via $\Gamma_D$ and Eq. (3), the resistivity via Eq. (4) and $\Gamma_D$ we correlate them with the electronic quantities of the metal. In the case of polycrystalline material for the accurate determination of the MFP, Eq. (5) should be modified as [177]:

$$MFP = \frac{0.75\pi}{(m^*e)^{1/3}} \frac{\hbar^*a_{pu}^{3/2}}{\Gamma_D - \Gamma_{\text{MFP}}}$$

(12)

where $\Gamma_{\text{MFP}}$ is the Drude broadening of the single-crystal nitride. However, for our analysis we are using Eq. (5) instead of Eq. (12) because $\Gamma_D$ values are not readily available, and thus, we are underestimating the actual MFP. These correlations are presented in Fig. 25. $E_{pu}$ and $\Gamma_D$ values exhibit broad scattering, mostly for TiN and TaN. The scattering for TiN is due to the variations of stoichiometry and grain morphology as noted in Table 3; indeed, values for fully dense stoichiometric TiN and fibrous overstoichiometric TiN$_{1.1}$ from Ref. [176] are included in Fig. 25, and constitute marginal cases of high and low quality TiN. On the other hand, the scattering for TaN is due to its metastable nature and the difficulty of producing pure B1-TaN [381,386,410,498], so most of the reported dielectric function spectra in literature are originating from mixed B1 and hexagonal phases of TaN. Consequently, in Fig. 25 and for the case of TaN the points corresponding to B1-TaN are distinguished from those for mixed phase samples by horizontal dotted lines. The magenta lines in Fig. 25 are guides to the eye drawn through the average values of each quantity for every nitride. $E_{pu}$ and $\Gamma_D$ values are rationally grouped according to the metal's period and group (i.e. to the principal quantum number and number of valence electrons) presented in Table 3. The yellow vertical lines are guides to the eye for mixed B1-TaN phases, the green horizontal dotted lines. The magenta lines in Fig. 25 are guides to the eye drawn through the average values of each quantity for every nitride. $E_{pu}$ and $\Gamma_D$ values are rationally grouped according to the metal's period and group (i.e. to the principal quantum number and number of valence electrons) presented in Table 3. The yellow vertical lines are guides to the eye for mixed B1-TaN phases, the green horizontal dotted lines.
electrons (which is increasing with increasing number of metal’s valence electrons) constitute the Fermi gas. A major exception is B1-WN; in particular, the PLD-grown B1-WN follows the computational trends for $E_{pu}$ and $G_D$, while sputtered B1-WN exhibit lower $E_{pu}$ due to the stoichiometry variations originating from the generation of point defects, which stabilize the B1 structure. The direct consequence of the observed variations of $E_{pu}$ and $G_D$ is the substantial increase of resistivity with increasing group number and the subsequent reduction of MFP of conduction electrons in agreement with the computational results of Fig. 16a and b.

As a partial conclusion, we observe that the less optically lossy nitrides are those of group IVb metals (TiN, ZrN, HfN). Among them, ZrN shows the smallest average value of $G_D$, which in combination with the minimized dielectric losses, as discussed previously, is emerging as the most promising refractory conductor. Therefore, ZrN nanostructures are foreseen to exhibit the best plasmonic performance. In addition, TiN and ZrN exhibit small and large work function, respectively, while they have similar melting points and $E_{pu}$, which are associated with conduction electron density (Fig. 26). Therefore, they can constitute a platform of tunable plasmonic conductors for hot electron applications. Regarding the nitrides of Vb metals, they exhibit higher conduction electron density and $E_{pu}$ compared to group Vb nitrides, and thus a plasmonic performance towards UV is predicted. They all exhibit $E_{pu}$, $G_D$ and MFP values similar to each other in the B1 structure. Given the metastable character of B1-TaN in contrast to the ease of fabricating epitaxial B1-NbN, we can safely conclude that for UV plasmonic applications B1-NbN is the most promising candidate.

2.2.5. Experimental dielectric function spectra of ternary nitrides

As we have seen and discussed, there are certain spectral limitations on the use of binary TMN for various applications. In particular, $\lambda_{ps}$ of binary TMN can be hardly extended beyond 600 nm, while the extension towards UV is hard due to the metastability and structural degradation of most nitrides of group Vb and Vb metals. Alloying and forming ternary TMN, with TiN or ZrN as basis, has been proposed as viable solutions to these two limitations. Thus, the conduction electron density, and consequently $E_{ps}$ and $\lambda_{ps}$ as well, can be quite accurately tuned by varying the effective number of valence electrons.
electrons of the constituent metals in Ti_xMe_1-xNo_rZ_r xMe_1-xN (where Me can be either a group IIb, IIIb, and IIIa element or a group Vb and VIb element):

\[ N_{eff} = \frac{x}{V_1} + (1-x) \cdot \frac{V_2}{C_1 V_2} \]

where \( V_1 \) is four for Ti or Zr (\( d^2s^2 \) valence electrons) and \( V_2 \) is the number of electrons of the alloying elements, which is two for Mg, Ca, three for Sc, Y, La, and Al, five for Nb, and Ta, and six for Mo. The spectra of the real (\( \epsilon_1 \)) and imaginary (\( \epsilon_2 \)) parts of the dielectric functions of a wide variety of ternary nitrides, grown by various techniques, such as hybrid CVA (HCVA), DIBS, MS and PLD, and which were originally reported in Refs. [184,439,471], are presented in Figs. 27 and 28, respectively. The \( E_{ps} \) and \( \Gamma_p \) values resulted from the fits by Eq. (11), as well as the resistivity and MFP values determined using Eqs. (4) and (5) are summarized in Table 5. All the spectra of Figs. 27 and 28 are for polycrystalline samples, so their electron losses are expected to be affected accordingly. The fit results from Ti_xLa_1-xN films are also summarized in Table 5, while the corresponding spectra are not included in Figs. 27 and 28 but can be found in Ref. [441,471]. Ti_xLa_1-xN films are amorphous due to the large lattice mismatch of the constituents (TiN and LaN). All the presented spectra are characteristic of good conductors, with the major exception of Ti_xMo_1-xN. In the latter case of Ti_xMo_1-xN the \( \epsilon_1 \) for wavelengths longer than \( \lambda_{ps} \) gets very small negative values, which are indicative of excessive electron loss. These films were not found to consist by the B1 phase, although they were grown with identical conditions with TiN. This can be attributed to the inherent metastable character of the B1-MoN and the intrinsic structural defects that are formed in B1-MoN [186,387]. Therefore, Ti atoms into Ti_xMo_1-xN are not as effective stabilizers of the B1 phase as in the case of B1-Ti_xTa_1-xN. Further work is required to clarify this issue.

The basic features of all spectra are the redshift of \( \lambda_{ps} \) (i.e. reduction of \( E_{ps} \)) when alloying TiN or ZrN with group II or group III elements, and the blueshift of \( \lambda_{ps} \) (i.e. increasing of \( E_{ps} \)) when alloying with group Vb elements, as a direct consequence of the variation of the effective number of valence electrons of the constituent metals according to Eq. (13). This is clearly illustrated in Fig. 23, where a correlation of \( E_{ps} \) with \( N_{eff} \) is presented. Indeed, in Fig. 23 the scattering of the experimental points for ternary nitrides is less than for their binary counterparts, suggesting that alloying the B1 phase may be a more effective and controlled way of tuning \( E_{ps} \) than varying the composition and microstructure of binary TMN. In particular, the optical performance, in terms of \( E_{ps} \), of Ta-rich Ti_xTa_1-xN and Mo-rich Ti_xMo_1-xN is superior to their metastable binary counterparts, indicating that small amounts of Ti may stabilize the B1 structure (at least for the case of Ti_xTa_1-xN) and provide a viable candidate for violet and UV plasmonics. The correlation of the electron losses via \( \Gamma_p \), and the operation range via \( l_{ps} \) presented in Fig. 24, shows that the polycrystalline ternary nitrides exhibit similar electron losses with their binary counterparts, which are higher than those of the epitaxial or fully dense binary TMN. This observation suggests that there is no substantial alloying scattering in such ternary systems and that better tunable optical performance would be achieved, if such ternary nitrides were grown epitaxially. This provides a strong incentive to put more effort in the crystal growth technology of conductive ternary TMN. With the current view of Fig. 24, the electron losses

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**Fig. 20.** Extrapolated \( \epsilon_1 \) spectra in the 350–1300 nm wavelength of light using the best fit value parameters presented in Table 3 for (a) TiN, (b) ZrN, (c) HfN, (d) VN, (e) NbN, (f) TaN, (g) MoN, and (h) WN; the fits were performed on experimental spectra reported by various groups worldwide (References presented in detail in Table 3); note that the spectra for TaN by Aouadi and Waechter coincide.
are minimized in the visible spectral range of $\lambda_{ps}$, while extensions of the operating range towards both UV and infrared come in expense of the electron losses. This has to be taken into account when designing optical devices based on ternary TMN.

A better evaluation of the optical performance of the various ternary nitrides can be done based on the correlations of $E_{pu}$, $G_D$, resistivity and MFP vs. the $N_{eff}$ as presented in Fig. 29. $E_{pu}$ (we remind that it is correlated with the conduction electron density) and $G_D$ are rationally increasing with $N_{eff}$ for all binary and ternary TMN in the B1 structure, in agreement with the computational results presented previously. TaN and Ti$_x$Mo$_{1-x}$N samples that do not consist exclusively of the B1 phase are distinguished by the dotted black line and they exhibit substantially lower $E_{pu}$ and carrier density than the B1 samples. For $N_{eff}$ between four and five, fully dense samples of low electron losses and resistivity can be developed in the Ti$_x$Ta$_{1-x}$N system. These samples are expected to exhibit plasmonic behavior at shorter wavelengths than TiN and ZrN. Note that the Zr$_x$Ta$_{1-x}$N exhibits smaller $E_{pu}$ (carrier density) and higher electron losses and resistivity compared to Ti$_x$Ta$_{1-x}$N of similar $N_{eff}$. This observation indicates that, despite of ZrN being a better optical conductor than TiN in its own merit, as we have already discussed, it is a less effective alloying constituent than TiN. This is possibly due to the large size of the cubic cell of B1-ZrN that is mismatched with most of the rest of TMN thus resulting to finer grains when alloyed to form ZrN-based ternary TMN. It could also be due to the large atomic mass of Zr that usually results in a higher amount of intrinsic stress and structural defects than TiN grown with similar conditions, mostly for kinetic reasons [309]. It seems that for $N_{eff} > 5$ all TMN exhibit excessive electron losses and high resistivity values, which make their perspectives for applications in plasmonics quite questionable. However, the relevant available experimental points are rather few to provide a solid conclusion on this issue.

For $N_{eff}$ below four, several alloying elements have been investigated. Among them, Ti$_x$Sc$_{1-x}$N emerges as the most...
promising system due to the overall lower electron losses and resistivity, and $E_{pu}$ values that are compatible with fully dense films with very few structural defects [471]. This is due to a combination of reasons such as the good lattice match between TiN and ScN, their structural compatibility (both TiN and ScN are stable in the B1 structure), and the similar valence electron configuration (d$^2$s$^2$ for Ti, d$^1$s$^2$ for Sc) and bonding with nitrogen. The main drawback of the Ti$_x$Sc$_{1-x}$N system is the very limited abundance of Sc in Earth’s crust, and the associated high cost of raw materials. An alternative and abundant candidate would be Ti$_x$Mg$_{1-x}$N, which exhibits the second best performance in terms of $E_{pu}, \Gamma_D, \text{resistivity and MFP in this } N_{\text{eff}} \text{ range. Although Mg is not soluble into TiN in the entire compositional range [471], there is a sufficient solubility range (mostly due to the similar atomic radii of Ti and Mg) where B1-Ti$_x$Mg$_{1-x}$N with plasmonic performance in the near infrared can be grown [441].}

The correlation of the conduction electron (carrier) density $N$ with the cell size of the various ternary nitrides is very important for applications involving heteroepitaxial structures. Fig. 30 shows the variation of $E_{pu}$ and $N$ (calculated from $E_{pu}$ according to Eq. (1)) vs. the lattice constant of the various binary and ternary nitrides in the B1 cubic phase. Open points correspond to representative conductive nitrides grown by PLD in Ref. [184] and having $N_{\text{eff}} \geq 4$; note that the binary nitrides are included in these sets of ternary data for $x = 0$, i.e. are the extreme value points of each set. Magenta stars correspond to the Ti$_x$Al$_{1-x}$N with $N_{\text{eff}} < 4$ reported in Ref. [453]. Finally solid symbols correspond to Ti$_x$Sc$_{1-x}$N, Ti$_x$Y$_{1-x}$N, Ti$_x$Mg$_{1-x}$N, and Ti$_x$Ca$_{1-x}$N (Ti$_x$La$_{1-x}$N is excluded from this
comparison because it is amorphous for the most cases) reported in Ref. [471] and having $N_{\text{eff}} < 4$, as well. ZrN exhibits the larger cubic cell size among all. The $E_{\text{pu}}$ values of each ternary nitride system follow almost linear correlations with the lattice constant and the composition $x$ of the films. All the ternary nitrides with Vb and IVb group elements exhibit higher $E_{\text{pu}}$ values than the Ti$_x$Zr$_{1-x}$N system due to the additional valence electrons of the constituent metals and, thus, they cover the upper part of the phase space. The Ti$_x$Al$_{1-x}$N system exhibits both smaller $E_{\text{pu}}$ and lattice size values compared to Ti$_x$Zr$_{1-x}$N. Using the experimental data for Ti$_x$Al$_{1-x}$N and the calculated lattice size of B1-AlN [585] we can conclude that Ti$_x$Al$_{1-x}$N can be grown fully dense, since the experimental points (magenta stars) coincide with the theoretical magenta line. On the other hand, the Ti$_x$Sc$_{1-x}$N, Ti$_x$Y$_{1-x}$N, Ti$_x$Mg$_{1-x}$N, and Ti$_x$Ca$_{1-x}$N systems cover a lattice size range comparable with the Ti$_x$Zr$_{1-x}$N system, while they exhibit substantially lower $E_{\text{pu}}$ values. Among them, the experimental values of the Ti$_x$Sc$_{1-x}$N system (black disks) are lying on the line (black line) that connects the TiN and ScN points, suggesting the formation of fully dense ternary compounds over the entire compositional range. On the contrary, the experimental $E_{\text{pu}}$ values of Ti$_x$Y$_{1-x}$N, Ti$_x$Mg$_{1-x}$N, and Ti$_x$Ca$_{1-x}$N (solid up and down triangles, and diamonds, respectively) are inferior to the predicted values (red and green lines, respectively), defined by the calculated lattice sizes of B1-YN [492], B1-MgN [586] and B1-CaN [587], further supporting the formation of underdense ternary compounds. Especially Ti$_x$Mg$_{1-x}$N and Ti$_x$Ca$_{1-x}$N, for high $x$-values, exhibit $E_{\text{pu}}^2$ values higher than TiN, indicating the existence of excess Mg and Ca atoms possibly in interstitial and not in substitutional positions.

Fig. 25. The variations of $E_{\text{pu}}$ and $\Gamma_\text{D}$, as determined by fitting the experimental spectra by Eq. (11), and as summarized in Table 4, and of the resistivity and the MFP, determined according to Eqs. (4) and (5), of binary nitrides vs. the atomic number of the constituent metal.

Fig. 26. The correlation of the WF of binary TMN with their melting point and $E_{\text{pu}}/\rho$ carrier concentration (disk diameter) in comparison with noble metals (red disks) and group IIIa metals (blue disks). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
Fig. 27. Spectra of the real part of the dielectric function (real permittivity) of a variety of ternary nitrides based on TiN and ZrN. First column: TMN consisting of a group II element (Mg, Ca) and a group IVb element (Ti). Second column: TMN consisting of a group IIIa element (Al) or a group IIIb element (Sc, Y) and a group IVb element (Ti, Zr). Third column: TMN consisting of two group IVb elements (Ti, Zr). Fourth column: TMN consisting of a group Vb element (Nb, Ta) and a group IVb element (Ti, Zr). Fifth column: TMN consisting of a group VIb element (Mo) and a group IVb element (Ti). In the low left corner the visual appearance of various ternary nitride samples. Data from Refs. [439,448,453,471].

Fig. 28. Spectra of the imaginary part of the dielectric function (imaginary permittivity) of a variety of ternary nitrides based on TiN and ZrN. First column: TMN consisting of a group II element (Mg, Ca) and a group IVb element (Ti). Second column: TMN consisting of a group IIIa element (Al) or a group IIIb element (Sc, Y) and a group IVb element (Ti, Zr). Third column: TMN consisting of two group IVb elements (Ti, Zr). Fourth column: TMN consisting of a group Vb element (Nb, Ta) and a group IVb element (Ti, Zr). Fifth column: TMN consisting of a group VIb element (Mo) and a group IVb element (Ti). Data from Refs. [439,448,453,471].
3. TMN nanostructures and plasmonic applications

3.1. Quality factors of plasmonic resonances

The dielectric function spectra (or complex permittivities), so far reviewed and studied in this work, are defining the plasmonic performance of the conductors. In principle, a conductor may sustain a plasmonic resonance, either an SPP at a planar interface or an LSPR in nanoparticles, at any given wavelength where $\varepsilon_1$ is negative; however, the quality of such resonance would be severely affected by the electron losses, which are mostly affected by $\varepsilon_2$. As a result, the most important question is not whether a resonance can be sustained but which is the quality of such resonance. Based on fundamental considerations, certain quality factors for SPP and LSPR have been established using $\varepsilon_1$ and $\varepsilon_2$ [168, 588]. In particular, for SPP at a planar interface between a planar TMN and a dielectric:

$$Q_{\text{SPP}} = \frac{\varepsilon_1 \cdot \text{TMN} + \varepsilon_1 \cdot d}{\varepsilon_1 \cdot \text{TMN} \cdot \frac{\varepsilon_2 \cdot \text{TMN}}{\varepsilon_1 \cdot d}}$$

and for spherical nanoparticles of TMN in air, the $Q_{\text{LSPR}}$:

$$Q_{\text{LSPR}} = \frac{-\varepsilon_1 \cdot \text{TMN}}{\varepsilon_2 \cdot \text{TMN}}$$

where $\varepsilon_1, \text{TMN}$ and $\varepsilon_2, \text{TMN}$ are the real and imaginary parts of the dielectric function of the TMN, and the $\varepsilon_1, d$ is the real part of the dielectric function of the adjacent dielectric ($\varepsilon_1, d = 1$ for air).

As a case study, we calculated the $Q_{\text{SPP}}$ for a thin TMN film adjacent to a thermal SiO$_2$ layer ($\varepsilon_1, d = \varepsilon_1, \text{SiO}_2 = 1.9$) for all the binary nitrides listed in Table 3 excluding the exceptionally lossy B$_1$-MoN and B$_1$-WN, and for the most promising ternary nitrides according to the data of Fig. 29. SiO$_2$ is chosen as an important demonstrator, as it is the major dielectric of Si microelectronics and of fiber optic telecommunications. The variations of $Q_{\text{SPP}}$ vs. the wavelength of the incoming light for binary and ternary nitrides are presented in Figs. 31 and 32, respectively. The vertical dotted lines in Fig. 31 separate the spectral range where $\varepsilon_1 < 0$ (intraband region) and $\varepsilon_1 > 0$ (interband region); the latter region has no physical importance and should be neglected. In Fig. 31 a strikingly difference of the $Q_{\text{SPP}}$ values between group IVb and Vb binary
nitrides is observed unequivocally proving the superior character of group IVb nitrides (TiN, ZrN, HfN) as plasmonic materials. Among them, the maximum $Q_{\text{SPP}}$ is observed for HfN, while the dielectric functions of more ZrN sample result in high $Q_{\text{SPP}}$ values, therefore, suggesting ZrN being the best plasmonic TMN taking into account the statistical significance of the measurements, as well. It seems that TiN is the worse among the three, albeit being the most widely studied so far. In addition, optimal $Q_{\text{SPP}}$ are observed for epitaxial and/or ultra-thin samples. Similar trends can ne identified for $Q_{\text{LSPR}}$ in Fig. 33, as well, albeit with less contrasting differences among the $Q_{\text{LSPR}}$ values of various binary TMN, suggesting that for LSPR applications, the range of viable plasmonic TMN can be wider.

Regarding the ternary TMN, the observed $Q_{\text{SPP}}$ (Fig. 32) and $Q_{\text{LSPR}}$ (Fig. 34) are optimal for Ti$_x$Ta$_{1-x}$N and Ti$_x$Sc$_{1-x}$N compared to Zr$_x$Ta$_{1-x}$N and Ti$_x$Mg$_{1-x}$N. The inferior $Q_{\text{SPP}}$ and $Q_{\text{LSPR}}$ for Zr$_x$Ta$_{1-x}$N compared to Ti$_x$Ta$_{1-x}$N confirms the previous discussion that although ZrN emerges as the most efficient plasmonic conductor on its own merit, it is a poor basis for alloying, possibly due to its long lattice cell size and the subsequent high lattice mismatch with the rest of TMN. However, this observation lacks statistical significance, as it is based on very few samples, and its general validity should be into scrutiny. Regarding the comparison between Ti$_x$Sc$_{1-x}$N and Ti$_x$Mg$_{1-x}$N, the superior performance of the former is attributed to the stability of the B1-ScN as alloying element and the electronic compatibility of Ti ($d^2s^2$ valence electrons) and Sc ($d^2s^2$ valence electrons). However, given the abundance of Mg, in contrast to the shortage of Sc, it is worth dedicating efforts for the improvement of its growth and plasmonic performance in order to implement it industrially.

Overall, the reported ternary TMN exhibit $Q_{\text{SPP}}$ and $Q_{\text{LSPR}}$ values comparable to polycrystalline and optically poorer binary group IVb TMN. Given that there is no systematic study of the optical properties and dielectric function spectra of epitaxial ternary TMN in the literature, their actual potential as plasmonic materials cannot be firmly evaluated given that the polycrystalline ternary TMN are usually of inferior crystalline quality, as presented in Section 2.2.4 and depicted in Fig. 5, and thus their inferior plasmonic performance can originate from the higher density of structural defects [384,471]. Therefore, a more systematic, experimental study of the optical properties of epitaxial ternary nitrides is of paramount importance in the field of alternative plasmonic materials.

\[ \text{Fig. 29.} E_{\text{pu}}, \Gamma_b, \text{resistivity, and MFP vs. the effective number of valence electrons of the constituent metals (N_{eff}). Solid and open symbols represent binary and ternary TMN, respectively.} \]
Fig. 30. The phase space of $E_{pu}^2$, which is proportional to the carrier (conduction electron) density, vs. the nitride’s lattice constant for the cubic B1 structure. Solid symbols represent the values of the systems with $N_{eff}<4$ studied in Refs. [471] and [453], while open symbols are for $N_{eff}/C21<4$ from Ref. [184]. Grey lines are guides to the eye, while colored straight lines connect the values for TiN with the calculated values of the corresponding binary nitride (B1-AlN, B1-ScN, etc).

Fig. 31. QSPP at the interface of binary TMN/SiO$_2$ vs. the wavelength of incoming light calculated using Eq. (14).
Fig. 32. $Q_{SPP}$ at the interface of representative ternary TMN/SiO$_2$ vs. the wavelength of incoming light calculated using Eq. (14).

Fig. 33. $Q_{LSPR}$ of binary TMN in air vs. the wavelength of incoming light calculated using Eq. (15).
A more quantitative picture of the plasmonic performance of TMN can be drawn from the maximum values of the quality factors $Q_{\text{SPP,max}}$ and $Q_{\text{LSPR,max}}$ for SPP and LSPR, respectively [588]. Under quasistatic conditions, i.e. where the feature size of a given plasmonic system is far smaller than the wavelength of the incoming light, which should be actually the case for any TMN due to their short MFP values (see Fig. 29) as we will discuss in more detail below, and for the case of minimum electron loss, i.e. for minimum $\epsilon_z$ which occurs at the spectral vicinity of $\lambda_{ps}$ as it is demonstrated in Figs. 19, 20 and 27, 28, $Q_{\text{SPP,max}}$ and $Q_{\text{LSPR,max}}$ can be expressed exclusively in terms of the $E_{pu}$ and $\Gamma_D$ parameters [588]:

$$Q_{\text{SPP,max}} = E_{pu}^2 / 2 \Gamma_D.$$  

$$Q_{\text{LSPR,max}} = G^2 / 2 \Gamma_D.$$
First we correlate the \(q_{SPP,max}\) and \(q_{LSPR,max}\) with the atomic number of the constituent metal of binary TMN (Fig. 35) in an effort to identify the intrinsic plasmonic potential of TMN due to their electronic structure. As there is substantial scattering of data for all TMN, we demonstrate with open circles the \(q_{SPP,max}\) and \(q_{LSPR,max}\) values of a set of binary TMN grown by PLD using identical conditions [184] in order to be directly comparable to each other. The \(q_{SPP,max}\) and \(q_{LSPR,max}\) of group IVb TMN are superior to the rest of the considered nitrides and similar to each other. ZrN and HfN are quite more effective than TiN for SPP, while their differences for LSPR are less pronounced. With increasing group number (and consequently increasing density of conduction electrons, as well) \(q_{SPP,max}\) and \(q_{LSPR,max}\) are substantially, and very reasonably, reduced. Having said that, we should take into account that this is not the complete story, as the reduced quality of a plasmonic resonance may be accompanied by the benefit of a substantial spectral shift. So the most complete view can emerge by correlating \(q_{SPP,max}\) and \(q_{LSPR,max}\) values with the \(\lambda_{ps}\), at whose spectral vicinity the plasmonic resonances are expected to occur; such a correlation for all the considered binary and ternary TMN of this work is presented in Fig. 36.

In Fig. 36, it is revealed that the optimal \(q_{SPP,max}\) and \(q_{LSPR,max}\) values are for group IVb TMN (TiN, ZrN, HfN) in epitaxial, fully dense and/or ultrathin forms, which however operate in the narrow \(\lambda_{ps}\) window of 390–510 nm (grey shade in Fig. 36). ZrN and HfN combine stronger resonances at shorter wavelengths compared to TiN. The rest of the binary nitrides exhibit inferior \(q_{SPP,max}\) and \(q_{LSPR,max}\) values compared to both TiN-ZrN-HfN and Ti-based ternary nitrides operating at the same \(\lambda_{ps}\). In particular, group VIb nitrides (MoN and WN) exhibit very poor \(q_{SPP,max}\) and \(q_{LSPR,max}\) values rendering them quite inappropriate for plasmonic applications, as they exhibit either no plasmonic enhancement at all (\(Q < 1\)) or very weak enhancement (\(1 < Q < 10\)). Especially the very lossy WN does not exhibit an LSPR at all (\(Q_{LSPR,max}\) is not a real number).

There is a similar picture of reducing \(q_{SPP,max}\) and \(q_{LSPR,max}\) when extending \(\lambda_{ps}\) towards UV, albeit for all different reasons. Indeed, reducing \(\lambda_{ps}\) is accompanied by increasing \(N_{off}\), which result in intrinsic enhancement of \(\Gamma_D\), for both binary and ternary TMN as it
is shown by the \textit{ab initio} calculations presented in Figs. 15 and 18, respectively. Adding to that the inferior crystalline quality of group Vb nitrides compared to IVb nitrides [439] and the degrading crystallinity of ternary nitrides by enriching with a group Vb element [384], as presented in Fig. 5, explains this behavior. Therefore, the reducing $Q_{\text{SSP,max}}$ and $Q_{\text{LSPR,max}}$ in the UV range, either for NbN, TaN or Ti$_x$Ta$_{1-x}$N come due to increased $\Gamma_D$ in contrast to the infrared range, where they are degrading due to reduced $\epsilon_{\pi\sigma}$. Any enhancement, either in the UV or infrared ranges, can be achieved by improving the crystalline quality of nitrides for plasmonics. In particular, the presented results clearly indicate that Ti$_x$Ta$_{1-x}$N performs better than NbN and TaN, suggesting that the addition of Ti into TaN stabilizes the B1 structure and reduce the structural defects affecting $\Gamma_D$. Further enhancement unequivocally calls for the epitaxial growth of such nitrides (VN, NbN, TaN, Ti$_x$Ta$_{1-x}$N and Ti$_x$Sc$_{1-x}$N) at high temperature and on lattice-matched dielectric substrates. The study of the optical properties of such epitaxial TMN by an accurate and straightforward technique such as spectroscopic ellipsometry, which is still missing in the literature, will clarify their actual potential for realistic plasmonic applications. Finally, the variation of $Q_{\text{SSP,max}}$ and $Q_{\text{LSPR,max}}$ values among various TMN is less than $Q_{\text{SSP,max}}$ suggesting that for LSPR applications the selection of nitride might be less critical than for SSP applications, and other assets than quality factor such as spectral operation, work function, lattice size (for heteropitaxy) and melting point may become prevalent.

The $Q_{\text{SSP,max}}$ and $Q_{\text{LSPR,max}}$ values of all the considered ternary nitrides are orders of magnitude inferior to the values reported for Ag and Au [588]; however, the reported $Q_{\text{SSP,max}}$ and $Q_{\text{LSPR,max}}$ values for Ag and Au [588] refer to highly crystalline metals with grain size larger than 300 nm [524], while most of the studied nitride samples consist of ultrafine grains less than 20 nm long [439, 441]. Therefore, a fair comparison would be to the Ag and Au of the same grain size; in that case, the ternary nitrides are still inferior but their plasmonic performance is comparable in the same order of magnitude to Au and Ag [439]. We will come back later to this issue. Likewise, Al might be a more efficient plasmonic material in the UV [148] than Ti$_x$Ta$_{1-x}$N, but this is accompanied by its tendency to oxidize fast [148] and its low melting point, two major drawbacks for realistic applications, especially when high photon fluxes are necessary [183]. Thus, Ti$_x$Ta$_{1-x}$N is emerging as a viable and stable candidate for UV plasmonics.

### 3.2. SPP performance at TMN/dielectric interfaces

The $Q_{\text{SSP,max}}$ and $Q_{\text{LSPR,max}}$ as expressed in Eqs. (16) and (17) and as displayed in Fig. 36 vs. $\lambda_0$ provide an indication of the intrinsic plasmonic properties of the conductor as it is based on quantities associated with bulk plasmons into the corresponding conductors, but cannot describe entirely and accurately the SSP and LSPR phenomena as they neglect the contribution of the adjacent dielectric (especially for SSP that occurs at conductor dielectric interfaces when illuminated via the dielectric) and of the geometry of the device (e.g. size and shape of nanoparticles for LSPR).

Therefore, a more realistic view of the potential of TMN for SSP applications can be extracted from the dispersion relation that correlates the frequency $\omega$ with the wave vector $k_s$ in the direction of propagation of SSP, in such a configuration, \textit{i.e.} along a conductor/dielectric interface. The general equation that defines the aforementioned relation is the following [1]:

$$k_s = \frac{\omega}{c} \sqrt{\frac{\epsilon_{\text{TMN}} - \epsilon_d}{\epsilon_{\text{TMN}} + \epsilon_d}}$$

(18)

where $\epsilon_{\text{TMN}}$ and $\epsilon_d$ are the complex dielectric functions of the TMN and the dielectric, respectively. Given that the dielectric functions are inherently complex, Eq. (18) should be modified to:

$$k_s = \frac{\omega}{c} \text{Re} \left( \sqrt{\frac{\epsilon_{\text{TMN}} - \epsilon_d}{\epsilon_{\text{TMN}} + \epsilon_d}} \right)$$

(19)

when optical attenuation in the conductor exists; this is very important for the conductive nitrides, due to their strong electron losses. A more convenient way of writing the dispersion relation in order to be more easily compared to the experiments is:

$$\hbar k_{sc} = \hbar \omega - \text{Re} \left( \sqrt{\frac{\epsilon_{\text{TMN}} - \epsilon_d}{\epsilon_{\text{TMN}} + \epsilon_d}} \right)$$

(20)

Fig. 37 presents the case study of calculated (via Eq. (20)) SSP dispersion relations at the interfaces between w-AlN and (a) TiN and the TiN-based ternaries that exhibit the optimal $Q_{\text{SSP,max}}$, and (b) group Vb TMN (TiN, ZrN, HfN). w-AlN was selected for this case study as a dielectric material with very wide range of transparency (see Fig. 38) and an almost constant refractive index and dielectric function in the entire range of plasmonic operation of TiN, ZrN, HfN, and TiN-based ternary TMN; in addition, w-AlN is a proven effective dielectric for SSP devices [589] and can be structurally compatible with TMN as w-AlN[0002]/TMN[111] can be grown pseudopitaxially, similar to GaN[0002]/TMN[111], which is reported in Ref. [224] and shown in Fig. 2b.

The first significant observation is that in all cases the dispersion relations are characteristic of lossy metals and, therefore, involve finite extreme values of $k_s$ [1] due to conduction electron (due to finite $\Gamma_D$ values of all ternary nitrides) and dielectric (due to the existence of interband transitions) losses. The consequence of this observation is the existence of quasi-bound modes at which the slope of the dispersion curve is inverted and the existence of a cross-over energy at which the SSP dispersion curve crosses the photon line (black straight lines). The maximum $\hbar k_{sc}$ below the light line defines the resonance point, which occurs for incoming light with the corresponding photon energy ($\lambda$-axis in Fig. 37). It is evident from Fig. 37a that by varying the microstructure and/or stoichiometry of TiN, SSP resonances in the light range of 1.6–2.3 eV (775–539 nm) can be achieved (yellow region in Fig. 37a). In order to probe effectively resonances beyond this range to either directions, TiN should be alloyed either with TaN or ScN to form Ti$_x$Ta$_{1-x}$N and Ti$_x$Sc$_{1-x}$N, respectively. Thus, SSP resonances up to 2.57 eV (482 nm), represented by the blue region in Fig. 37a, or down to 1.19 eV (1042 nm) represented by the grey region in Fig. 37a, can take place.

On the other hand, comparing TiN with ZrN and HfN (Fig. 37b) reveals that these three nitrides can sustain resonances in an overlapping range (yellow region in Fig. 37b); ZrN's resonances extent slightly towards blue (yellow region in Fig. 37b), but still not as far as Ti$_x$Ta$_{1-x}$N's. This similarity is a consequence of their similar $E_{\pi\sigma}$ values as we have shown in Fig. 29. Their major difference is the maximum $\hbar k_{sc}$ that is 5.5, 7.5 and 7 eV for TiN, HfN, and ZrN, respectively, and represented by light, intermediate and dark grey regions in Fig. 37b. This behavior is attributed to the gradually less dielectric losses of TiN, HfN, and ZrN as revealed by the comparison of their dielectric function spectra in Fig. 21. As a result, an SSP at the resonance point on a ZrN/w-AlN interface will have shorter wavelength than on a TiN/w-AlN interface making ZrN more appropriate for sub-wavelength optics. The less losses for ZrN compared to TiN also result in longer propagation lengths $L_{\text{SSP}}$, which may be given by [590]:

$$L_{\text{SSP}} = \lambda_{\text{light}} \frac{\epsilon_{1,\text{TMN}}^2}{2\pi \epsilon_{2,\text{TMN}}} \left( \frac{\epsilon_{1,\text{TMN}} + \epsilon_{1,d}}{\epsilon_{1,\text{TMN}} \cdot \epsilon_{1,d}} \right)^{\frac{3}{2}}$$

(21)
For example, for the usual telecom wavelength of $\lambda_{\text{light}} = 1350$ nm, the propagation wavelength of SPP for TiN and ZrN is 2.5 $\mu$m and 6 $\mu$m, respectively; both are exceptionally short and this should be taken into account in any device design.

Of special importance for a variety of applications, predominantly for telecommunications [441] and for biosensing [591], as well, are plasmonic devices operating in the near infrared range (700–1600 nm). This spectral range is overlapping and adjacent to the wide range of transparency of most inorganic dielectrics and semiconductors spanning from 1100 to 5500 nm [592–595], as shown in Fig. 38 where the refractive index spectra of the most popular dielectrics and semiconductors reported in Ref. [592–597] are summarized. The combined 700–5500 nm near infrared range includes the well known biological window (where tissues, blood, and fat are transparent [591]) and the telecom window, which includes the 850, 1300/1550 nm bands used in fiber-optics and Si

Fig. 37. SPP dispersion relations for (a) TiN and the TiN-based ternaries that exhibit the optimal $Q_{\text{SPP,max}}$, and (b) group IVb TMN (TiN, ZrN, HfN) in contact with a w-AlN dielectric.
Fig. 38. Refractive index spectra of the most common inorganic dielectrics and semiconductors. Polar compounds are not transparent for wavelengths longer than 5500 nm due to polarity vibrations. A wide part of this range (1155–5500 nm and beyond) is covered by Si, for shorter wavelengths transparent dielectrics include nitriles (down to 200 nm for w-AlN) and oxides (MgO, quartz and sapphire being transparent below 200 nm). The biological and telecom windows are indicated by red and green shadows respectively. The most common telecom bands (850, 1300, 1550 nm) are also indicated by vertical dashed black lines. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Fig. 39. SPP dispersion relations at the nitride/dielectric interfaces for air and the two most widely used dielectrics in telecom technologies, i.e. silica and silicon for: (a) Ti_xSc_(1-x)N, (b) Ti_xY_(1-x)N, (c) Ti_xMg_(1-x)N, (d) Ti_xAl_(1-x)N, and (e) Ti_xCa_(1-x)N; the black lines are the dispersion relations of the light into the dielectrics; horizontal grey lines indicate the three bands used for telecommunications with today’s technology. (f) The scaling of the free space wavelength of light at SPP, which corresponds to the maximum $h \kappa c$ with $\lambda_{pe}$.
telecoms, respectively [598]. Therefore, materials that can sustain plasmonic resonances in this range are technologically essential. As a second case study we evaluate the SPP performance of ternary TMN with $N_{eff} < 4$ in contact with SiO$_2$ or Si, in order to investigate their suitability for telecom applications [441]. Fig. 39 presents the calculated (via Eq. (20)) SPP dispersion relations at the interfaces between air, silica or silicon and (a) Ti$_x$Sc$_{1-x}$N, (b) Ti$_x$Y$_{1-x}$N, (c) Ti$_x$Mg$_{1-x}$N, (d) Ti$_x$Al$_{1-x}$N, and (e) Ti$_x$Ca$_{1-x}$N, respectively. Note that the calculation for silicon was performed only for the transparent region, i.e. for photon energies in free space below the band gap of 1.112 eV (wavelength longer than 1115 nm), which lies exclusively in the infrared spectral range. All nitrides of this category behave like lossy conductors as their counterparts presented in Fig. 37. The photon energy that corresponds to the maximum $\epsilon_k c_{\text{max}}$, which defines the SPP point, is scaled to $\lambda_{\text{ps}}$ for all the ternary nitrides in the infrared spectral range; this is clearly illustrated for the silica dielectric in Fig. 39. However, these two quantities do not coincide and the wavelength of photons in free space that corresponds to $\epsilon_k c_{\text{max}}$ is longer than the wavelength $\lambda_{\text{ps}}$ and fulfills the requirement for operation at 850 nm for silica fiber optics when Ti$_{0.32}$Sc$_{0.68}$N is used, while Ti$_{0.73}$Mg$_{0.27}$N and Ti$_{0.75}$Ca$_{0.25}$N are also pretty close to fulfill this requirement possibly with a small further enrichment with Mg or Ca. Air can hardly sustain a SPP mode for all cases, while clear SPP is observed for silica albeit at shorter wavelengths than the 850 nm telecom band in most cases with the major exception of Ti$_x$Sc$_{1-x}$N.

The inability to meet the requirement of 850 nm wavelength is not a deficit of the experimental range reported in Ref. [441], but it is also due to physical limitations for various ternary conductive nitrides; for example further enrichment with Al or Y in order to extend the range of operation of Ti$_x$Al$_{1-x}$N and Ti$_x$Y$_{1-x}$N would cause a phase transition from the B1 phase to pseudo-wurtzite [453] or further grain refinement due to the lattice mismatch between TiN and YN [471], respectively, while Ti$_x$Ca$_{1-x}$N is characterized by inherent excessive electron loss [471]. The only family of conductive nitrides that can sustain a SPP for the silicon telecom bands (1300 nm and 1550 nm) is the Sc-rich Ti$_x$Sc$_{1-x}$N, while for the silica fiber band (850 nm) both Ti$_x$Sc$_{1-x}$N and Ti$_x$Mg$_{1-x}$N might be considered. The later is inferior in terms of the quality factor $Q_{\text{SPP,max}}$, as we have already discussed, but given the abundance of Mg, in contrast to the shortage of Sc, it is worth dedicating efforts for the improvement of its growth and plasmonic performance in order to implement it industrially.

3.3. LSPR performance of TMN nanoparticles

3.3.1. Far field properties

Having a massive volume of optical data for binary and ternary TMN may enable us to evaluate the expected LSPR performance of the hypothetical equivalent nanoparticles via the by Maxwell-Garnett Effective Medium Approximation (MG-EMA) [15]. Although MG-EMA is not as accurate as the exact Finite Difference Time Domain (FDTD) calculations and lacks the versatility of the later regarding the shape of nanoparticles or nanoantenas, it might provide a reasonable and effective preliminary comparison of the various binary and ternary nitrides. Otherwise, such a critical comparison would require an immense experimental effort in an unrealistic scale. Indeed, the far-field optical response of spherical TMN nanoparticle assemblies can be reasonably described by MG-EMA:

$$\frac{\tilde{\varepsilon} - \tilde{\varepsilon}_{\text{TMN}}}{\tilde{\varepsilon} + 2\tilde{\varepsilon}_{\text{TMN}}} = f_{\text{TMN}} \frac{\tilde{\varepsilon}_{\text{TMN}} - \tilde{\varepsilon}_d}{\tilde{\varepsilon} + 2\tilde{\varepsilon}_{\text{TMN}}}$$

(22)
which describes the effective complex dielectric function \( \tilde{\varepsilon} \) of a composite material consisting of a dielectric host (matrix) with complex dielectric function \( \tilde{\varepsilon}_d \) and isolated spherical inclusions of the secondary phase (TMN in our case) having complex dielectric function \( \tilde{\varepsilon}_{TMN} \) with a filling ratio \( f_{TMN} \). The information of particle size is introduced via \( \tilde{\varepsilon}_{TMN} \) through the MFP, given that for small particles (up to 40 nm) these quantities are closely related \[551\].

As a case study we consider \( \tilde{\varepsilon}_d = 1 \) assuming air as the host medium. The \( \varepsilon_1 \) and \( \varepsilon_2 \) spectra of binary TMN nanoparticle assemblies in air with filling ratio \( f_{TMN} = 10\% \) vol calculated by MG-EMA are presented in Figs. 40 and 41, respectively. Note that MoN and WN are excluded from this comparison because of their poor QLSPR,max values. The LSPR is spectrally located at the wavelength where the \( \varepsilon_2 \) of the nanoparticles gets the maximum value. Stronger and sharper resonances are observed for group IVb nitrides, and in particular for ZrN and HfN, which are also moderately blueshifted compared to the resonances for TiN; indeed, ZrN is emerging as the most efficient TMN for LSPR applications. Among group VB nitrides, NbN exhibits by far the stronger and sharper resonances, which are comparable to medium-quality TiN, albeit substantially blueshifted.

The spectral position of the LSPR of TMN nanoparticles is scaled with the \( \lambda_{ps} \) of the opaque, continuous TMN films, as presented in Fig. 42. There is remarkable low scattering of the points with very few samples not following the linear trend. The solid line is a linear fit to the data, while the dashed line stands for \( \lambda_{LSPR} = \lambda_{ps} \). The two lines are parallel and \( \lambda_{LSPR} \) is longer than \( \lambda_{ps} \) by 40 nm. This firm and quantitative scaling may provide a design tool for plasmonic devices based on TMN, especially for top-down fabrication, such as nanoinprint lithography combined with reactive ion etching of continuous TMN films (whose \( \lambda_{ps} \) can be known before patterning) \[599\].

The asset of the refractory character and thermal stability of TMN comes with the liability of the growth of fine grains. Thus, the range of spectral tunability via tailoring of size of TMN nanostructures, which is common practice for Au and Ag nanostructures nanoantennas \[600\], is very limited. Indeed, in most cases of TMN the MFP is less than 40 nm and in exceptional cases of epitaxial nitrides may be as long as 100 nm \( \lambda_{ps} \). Producing nanoantennas longer than the MFP of the nitride would not perform adequately and would not result in spectral plasmonic tunability. This drawback was recently addressed by introducing ternary TMN as tunable plasmonic materials \[439\].

MG-EMA calculations of the optical response of representative hypothetical nanoparticles of ternary nitrides in air with a filling ratio 10% vol are presented in Fig. 43. In particular, we present the \( \varepsilon_1, \varepsilon_2 \) spectra of polycrystalline nanoparticles modelled by DIBS-grown Ti\(_x\)Ta\(_{1-x}\)N (Fig. 43a,b), and MS-grown Ti\(_x\)Ta\(_{1-x}\)N and Ti\(_x\)Al\(_{1-x}\)N (Fig. 43c,d), and single-cystal nanoparticles modelled by epitaxial Ti\(_x\)Sc\(_{1-x}\)N (Fig. 43e,f) using the reference dielectric function spectra of opaque continuous Ti\(_x\)Ta\(_{1-x}\)N and Ti\(_x\)Al\(_{1-x}\)N films presented in Fig. 27 and 28. For the latter case (single-crystal Ti\(_x\)Sc\(_{1-x}\)N) the reference dielectric function spectra were extracted by analyzing the optical reflectivity spectra presented in the inset of Fig. 43e and retrieved and reproduced from Ref. \[469\].

The \( \lambda_{LSPR} \) of all ternary TMN (not only those presented in Fig. 43) follows the scaling relation of their binary counterparts with \( \lambda_{ps} \) and extend the operational range towards UV (open magenta symbols standing for various types of Ti\(_x\)Ta\(_{1-x}\)N) and towards infrared (open wine circles and open red squares standing for Ti\(_x\)Sc\(_{1-x}\)).
Given that $\lambda_{LSPR}$ and $E_{ps}$ are strongly correlated with the effective number of valence electrons of the constituent metals (Fig. 23), the importance of $N_{eff}$ to the LSPR spectral location is indirectly revealed. Thus, when TiN is alloyed with TaN, which has substantially higher conduction electron density, to form Ti$_x$Ta$_{1-x}$N the LSPR wavelength is gradually blueshifted with increasing Ta content. On the contrary, when Al or Sc is incorporated into TiN to form Ti$_x$Al$_{1-x}$N or Ti$_x$Sc$_{1-x}$N the conduction electron density is reduced and, consequently, the LSPR is redshifted. Ti$_x$Sc$_{1-x}$N exhibit sharper LSPR and spans deeper into the infrared than Ti$_x$Al$_{1-x}$N due to the structural, electronic and chemical compatibility with TiN as we have already discussed. An additional asset of ternary TMN nanostructures, especially Ti$_x$Sc$_{1-x}$N, which operates in the infrared range, is that can be spectrally tunable while retaining miniature size of a few tens of nm in contrast to noble metal nanoantennas [600] or nanoparticles [132], which require a feature size an order of magnitude larger, i.e. a few hundreds of nm, in order to exhibit resonances in the infrared. Therefore, Ti$_x$Sc$_{1-x}$N might be more efficient for miniature infrared plasmonic devices, thus turning the liability of fine grains into an asset.

![Fig. 42. Scaling of the wavelength of incoming light where LSPR occurs ($\lambda_{LSPR}$) with the $\lambda_{ps}$ of the corresponding continuous nitride. The solid line is a linear fit to the data, while the dashed line stands for $\lambda_{LSPR} = \lambda_{ps}$.](image1)

![Fig. 43. $\varepsilon_1$, $\varepsilon_2$ spectra of hypothetical polycrystalline nanoparticles determined by MG-EMA (f$_{TMN} = 10%$ vol) using the reference dielectric functions of DIBS-grown Ti$_x$Ta$_{1-x}$N (a,b), MS-grown Ti$_x$Ta$_{1-x}$N and Ti$_x$Al$_{1-x}$N (c,d), and of hypothetical single-cystal nanoparticles using the reference dielectric functions of epitaxial Ti$_x$Sc$_{1-x}$N (e,f). Inset shows the raw optical data for Ti$_x$Sc$_{1-x}$N, as retrieved from Ref. [469], and the corresponding fit.](image2)
The strength of LSPR may be expressed by the actual $\varepsilon_2$ value at the resonance wavelength $\lambda_{\text{LSPR}}$ (see Fig. 44). Maximum strength is achieved for ZrN and HfN among all the considered TMN, however, only in the narrow spectral window 450–510 nm. For longer wavelengths (510–560 nm) TiN provides the stronger resonance, albeit far weaker than those of ZrN and HfN; for much longer wavelengths (>560 nm) firstly Ti$_x$Sc$_{1-x}$N and secondarily Ti$_x$Mg$_{1-x}$N are the most efficient conductors for LSPR. On the opposite side, for wavelengths shorter than 450 nm, Ti$_x$Ta$_{1-x}$N is the best candidate, NbN exhibits intermediate performance (which is anticipated to improve, if NbN is grown epitaxially), and TaN’s performance is very poor. As a partial conclusion, if the priority of spectral selectivity was of importance, a range of TMN that includes Ti$_x$Ta$_{1-x}$N, ZrN, TiN, and Ti$_x$Sc$_{1-x}$N would be considered.

Another open question is whether stronger and/or sharper resonances can be achieved by single-crystalline TMN nanoparticles compared to the polycrystalline nanoparticles mostly considered so far. In order to clarify this point we considered the dielectric functions of hypothetical Ti$_x$Sc$_{1-x}$N nanoparticles of varying $x$ calculated by MG-EMA using the reference dielectric functions of polycrystalline and epitaxial Ti$_x$Sc$_{1-x}$N films respectively [441]. From Fig. 45, it is evident that the polycrystalline Ti$_x$Sc$_{1-x}$N quite wider and a bit weaker resonances than the epitaxial Ti$_x$Sc$_{1-x}$N. By comparing polycrystalline and epitaxial Ti$_x$Sc$_{1-x}$N samples with almost the same $x$ values, we conclude that the use of epitaxial quality single-crystal nanoparticles exhibit sharper resonances, which are slightly redshifted with respect to those of the corresponding polycrystalline nanoparticles. This can be quantified by the Q-factor of the resonance [601]:

$$Q_{\text{factor}} = \frac{\lambda_{\text{LSPR}}}{\Delta \lambda},$$

which should not be confused with $Q_{\text{LSPR}}$ in Eq. (15); $\Delta \lambda$ is the bandwidth (full width at half maximum) of the resonance. The inset in Fig. 45 shows the variation of $Q_{\text{factor}}$ of Ti$_x$Sc$_{1-x}$N nanoparticles, polycrystalline or of epitaxial quality, with the wavelength of LSPR.

The epitaxial quality nanoparticles exhibit substantially higher Q-factor for all cases; however, Q-factor is reducing towards infrared even for the epitaxial quality nanoparticles due to reducing conduction electron density.

After this long story on the importance of TMN nanoparticles as plasmonic materials, we should provide a direct comparison with noble metals as a final assessment. A fair comparison would be among nanoparticles of the same size (radius) $r$. For ZrN and TiN we accept the assumption $2r = \text{MFP}$ and we use for MG-EMA dielectric functions that correspond to samples with $\text{MFP} \sim 40$ nm. For Au and Ag, the appropriate dielectric functions of nanoparticles should include the surface scattering contribution in the free electron relaxation time $\tau$ and $\Gamma_z$ parameter [139]:

$$\frac{1}{\tau_{\text{NP}}} = \frac{1}{\tau_{\text{bulk}}} + \frac{\Gamma_z}{\tau} \Rightarrow \Gamma_{z,\text{NP}} = \Gamma_{z,\text{bulk}} + \frac{\Gamma_z}{\tau},$$

where $\tau_{\text{NP}}$ and $\tau_{\text{bulk}}$ are the electron relaxation times, and $\Gamma_{z,\text{NP}}$ and $\Gamma_{z,\text{bulk}}$ are the Drude broadenings (expressed in Hz and not in eV as in the rest of this work) of the nanoparticles and the corresponding bulk metal, respectively, and $r$ is the particle radius (20 nm in our study to result in particle size of 40 nm) and $v_F$ is the Fermi velocity. The results of the MG-EMA calculations of the imaginary part $\varepsilon_2$ of the effective dielectric function of assemblies of nanoparticles of Au, Ag, TiN, and ZrN in air with 10% vol filling ratio are presented in Fig. 46. Au and TiN exhibit LSPR at very similar wavelengths, and the strengths of their resonances are comparable. Au’s LSPR exhibits sharper LSPR (higher Q-factor) but higher dielectric losses at short wavelengths, as well, than TiN making TiN’s LSPR more clear and well-shaped. ZrN exhibits stronger but wider LSPR than Au that makes it a very appealing candidate for a variety of plasmonic applications. Of course, none of them can compete Ag exclusively in terms of plasmonic performance. In conclusion ZrN and TiN exhibit broader LSPR than Au and Ag, as a result of their high electronic losses, but the strength of their LSPR is superior to Au. Taking into account all the rest of their assets (CMOS-compatibility, thermal stability, mechanical rigidity, etc), they definitely deserve to be implemented in various plasmonic devices.

### 3.3.2. Near field properties

The near field properties of representative binary and ternary TMN and the plasmonic enhancement provided by the TMN were studied using FDTD simulations (in which Maxwell equations are solved explicitly [602]) and presented in Fig. 48. For FDTD we used as input the experimental dielectric functions presented in Ref. [439]. We simulate an array of nanoparticles (40 nm diameter) suspended in air under plane wave illumination, for a wide range of volume filling ratios from ~5% up to ~45%. We extract the maximum intensity enhancement, which occurs at the nanoparticle surface (see inset of Fig. 48), for each plasmonic TMN and volume filling ratio. We observe that all TMN exhibit very similar plasmonic enhancements, irrespective of the volume filling ratio, and even more, this plasmonic response is somehow inferior, yet in the same order of magnitude, to the field enhancement of Au. It is
worth noting that the maximum field enhancement is almost constant for all TMN for the entire visible (400–700 nm) and UVA (315–400 nm). We thus conclude that TMNs offer an excellent platform for tunable plasmonic responses, with their near field effects being competitive, given their additional assets (mechanical and thermal stability, refractory character, varying work function), to the ones obtained by standard plasmonic metals such as Au, and with exceptional spectral tunability (Fig. 47).

3.3.3. Photothermal properties

High temperatures are developed inside plasmonic nanoparticles when they are irradiated by strong beams at their LSPR frequency, for example in applications in immunoassays [603], chemical and biological sensing [25,109,604–607] and surface enhanced spectroscopies [108,132,608–612]. Typically this is something to be avoided as it could result into nanoparticle reshaping [77,613–615] and thus into the destruction of the plasmonic template. The use of TMN nanoparticles, however, can uplift this limitation and open up a new window of opportunity into high-temperature plasmonic operation, involving simultaneous hot-electron and hot-lattice excitations. In this work we attempt a comprehensive theoretical evaluation of the TMN plasmonic response within a wide range of operating temperatures (300–3200 K) and compare it with the corresponding response of noble metals. Specifically, the bulk melting points of ZrN, TiN and TaN are a little over 3200 K [616] while the corresponding values for Ag and Au are 1236 K and 1338 K respectively and even lower for small nanoparticles (<40 nm diameter) [617,618].

We simulate a semi-infinite array of hemispherical nanoparticles on a Si substrate (including 2 nm of native SiO2), a structure typically used in surface enhanced spectroscopy applications [132]. We note that this is not the structure with maximal plasmonic enhancement but rather a standard model that makes our high-temperature study simpler. In our calculations we consider two TMN nanoparticles (TiN and ZrN) and two noble metals nanoparticles (Au and Ag) with a nanoparticle diameter of 40 nm arranged in a 44 nm square lattice (surface coverage 65%) within the 300–3200 K temperature range. We calculate the intensity enhancement in the middle of the gap between the nanoparticles under plane wave illumination in the spectral range of 0.3–3 μm. To do so we use the finite-difference time-domain (FDTD) method in which Maxwell’s equations including the material polarization are solved on a computational grid [139,602,619]. Material dielectric functions are inserted through a Drude-Lorentz polarizability model. The model’s parameters are

![Fig. 45. MG-EMA calculations of the ε₂ spectra of hypothetical polycrystalline and single-crystalline (epitaxial-quality) Ti₅Sc₁₋ₓN nanoparticles in air showing clear LSPR; the inset shows the Q-factor of the resonance, which is superior for epitaxial quality nanoparticles, and it is reducing as the resonance shifts towards infrared.](image1)

![Fig. 46. Spectra of the imaginary part of the dielectric function of 40 nm nanoparticles of Au, Ag, TiN, and ZrN in air with filling ratio 10% vol calculated by MG-EMA. The inset is a magnification of the spectra at the vicinity of the LSPR of Au and TiN.](image2)
fitted to the experimentally measured dielectric functions (TiN and ZrN from this work and also [439], Au [524] and Ag [522]). In order to get the appropriate dielectric constant for the nanoparticles, we need to include the surface scattering contribution in the free electron relaxation time [139] according to Eq. (24).

The goal of our study is to model the optical properties of the TMN and noble metal nanoparticles over a wide temperature range. The dominant effect of temperature is on the free electron relaxation time through the temperature dependence of the phonon population and of the crystal vacancies and imperfections [620,621]. Other, more minor effects such electron–electron scattering and small modifications of electron concentration due to nanoparticle volume expansion (which can cause a small redshift in the LSPR frequency) [620] or changes in the Fermi velocity ($k_B T/\sqrt{m^2_F}$ even close to melting [621]) are ignored for simplicity. We use a semi-empirical model for creating a temperature-dependent Drude-Lorentz model [622], via the electron relaxation time $\tau$, similarly to what has been used in previous theoretical works [622,623]:

$$\frac{1}{\tau(T)} = \frac{1}{\tau_0} \frac{T}{T_0} \alpha + \frac{v_F}{\tau},$$

(25)

where $T_0 = 300$ K and $T$ is the operating temperature. The parameter $\alpha$ should be fitted from thermal emissivity data [622,623]. Due to the lack of such experimental data for TMN and noble metals, however, we follow a simpler approach in which we assume that the temperature dependence of the optical (AC) relaxation time is similar to that of the static (DC) case. In the latter case the relaxation time is given by the Drude model $\tau_{DC}(T) \propto \rho(T)$ [624], thus the optical relaxation time is simply:

$$\frac{1}{\tau(T)} = \frac{1}{\tau_0} \frac{\rho(T)}{\rho(T_0)} \frac{v_F}{\tau},$$

(26)

We use $h \tau^{-1} = 0.068$ and $0.071$ eV for Au and Ag respectively at 300 K and literature data for $\rho(T)$ [625] and adjust the exponent $\alpha$ in Eq. (25). This empirical $\tau(T)$ is excellently fitted by the same $\alpha=1.14$ for the both metals, as shown in Fig. 48. This value is also in excellent agreement with literature values of the linear temperature coefficient of resistivity (TCR) $\alpha' = \alpha/T_0$ [625], as found after linearly expanding Eq. (25) ($T/T_0 = 1 + \alpha' \Delta T$), with $\alpha' = \alpha/T_0$ and $\Delta T = T - T_0$.

High temperature TMN electrical resistivity has not been studied in the literature. The available data to our knowledge for TiN [303,626,627] are found in the 10–400 K temperature range and in 10–300 K for ZrN [303,311]. The electrical resistivity in Eq. (25). This empirical $\tau(T)$ is excellently fitted by the same $\alpha=1.14$ for the both metals, as shown in Fig. 48. This value is also in excellent agreement with literature values of the linear temperature coefficient of resistivity (TCR) $\alpha' = \alpha/T_0$ [625], as found after linearly expanding Eq. (25) ($T/T_0 = 1 + \alpha' \Delta T$), with $\alpha' = \alpha/T_0$ and $\Delta T = T - T_0$.

High temperature TMN electrical resistivity has not been studied in the literature. The available data to our knowledge for TiN [303,626,627] are found in the 10–400 K temperature range and in 10–300 K for ZrN [303,311]. The electrical resistivity...
strongly depends on the TMN crystallinity, which in turn is related to the growth protocol. Specifically, the room temperature electrical resistivity of TiN is found to vary between 13 and 200 \( \mu \Omega \text{cm} \) for single crystal and polycrystalline films, while for ZrN the corresponding variation is between 12 and 2000 \( \mu \Omega \text{cm} \) [303]. We use the linear TCR at 300 K to get \( a = aT_{0} \) for TiN and ZrN. For polycrystalline films we get \( a \approx 1 \) [626] for both materials, while for single crystal films \( a = 1.2 \) is more appropriate [469] (a smaller coefficient points to a smaller effect of scattering from phonons compared to scattering from structural defects such as grain boundaries). In order to cover all ranges and possibilities, we consider the range \( a = 1-1.3 \). Using \( h\tau^{-1} = 0.35 \) and 0.33 eV for TiN and ZrN at 300 K (as obtained from the Drude-Lorentz fit of the ellipsometric data), we plot the corresponding \( \tau(T) \) in Fig. 48.

We extract from the FDTD solutions the electromagnetic fields at every point in the structure in time domain and by Fourier transforms we get the corresponding quantities in frequency domain [628]. The spectrally resolved intensity enhancement is calculated in the midgap position between the nanoparticles and is defined as \( |E(\omega)/E_{0}(\omega)|^{2} \) where \( E \) is the electric field at the specific point and \( E_{0} \) is the incident electric field. This is shown in Fig. 49 for TiN nanoparticles at different temperatures. The top inset depicts the simulated structure while the bottom inset shows the intensity distribution at the LSPR frequency at 300 K. For increasing temperature we observe a small redshift and a significant broadening that eventually flattens out the LSPR response. A similar response is found also for the nanoparticle absorption.

We attempt now a side-by-side comparison of the two nitrides with the two noble metals in a realistic high-power high-temperature operation. To do so we adopt the thermal transient heating calculations of Ag nanoparticles on Si under pulsed laser illumination that were conducted in a recent study for the same exactly system [615]. Specifically, it was found that under a Nd:YAG pulse at 532 nm with fluence \( f = 1 \text{ mJ/cm}^{2} \) (FWHM = 6 ns, peak power \( P_{\text{peak}} = 0.162 \text{ MW/cm}^{2} \)) the nanoparticle structure was heated up to a peak \( \Delta T = 1.75 \text{ K} \). The pulse profile is shown in the inset of Fig. 50b. We assume a linear dependence \( P_{\text{peak}}A(T) = \Gamma \Delta T \), where \( \Gamma \) is the thermal conductance between the nanoparticles and the Si substrate and \( A(T) \) the calculated nanoparticle absorption ratio at temperature \( T \). In [615] the absorption for the 40 nm Ag nanoparticles was calculated \( A(300 \text{ K}) = 0.14 \), from which we find \( \Gamma = 130 \text{ MW/m}^{2}\text{K} \). For simplicity we use this value for all materials hereafter. We can thus associate any given \( \Delta T \) to a \( P_{\text{peak}} \) and thus to an incident peak electric field \( |E_{\text{field,peak}} = (2z_{0}P_{\text{peak}})^{1/2} \), where \( z_{0} = 377 \Omega \) is the impedance of the free space. Furthermore, from the calculated intensity enhancement \( F(T) \) we get for the enhanced peak near-field \( |E_{\text{peak}} = |E_{0}\text{peak}|F(T)|^{1/2} = |2z_{0} \Gamma R(T) \Delta T/A(T)|^{1/2} \).

The peak near field and the corresponding \( \Delta T \) are plotted as a function of laser fluence in Fig. 50 for all four considered materials, each for the corresponding wavelength at which the LSPR appears at 300 K. We find that the E-field rises very quickly for the noble metals, but it is still comparable to that of the nitrides. We plot the response up to the corresponding melting point and as expected, the nitride nanoparticle response extends for up to much higher laser fluence, eventually providing for equally strong electric fields as that of the noble metals. What is most interesting in these results, we believe, is the possibility of finely tuning the nanoparticle temperature up to very high values making it an important parameter of the plasmonic response. For example, being able to access temperatures up to 3000 K, where \( k_{B}T = 0.26 \text{ eV} \), brings the nanoparticle thermal bath into the energy range of most molecule vibrational modes and thus potentially...

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Fig. 49. a) Simulated spectral intensity enhancement for TiN nanoparticles on Si assuming \( \alpha = 1 \). The top inset shows a schematic of the simulation system: 40 nm TiN hemispherical nanoparticles on top of a Si substrate, including a 2 nm native oxide. The Si substrate is for simplicity assumed to have a dielectric constant of 11.9, while the nanoparticles are arranged at a 44 nm period leaving 4 nm gaps in between them. The bottom inset shows the intensity distribution at the LSPR frequency for 300 K.

Fig. 50. The enhanced plasmonic near field for Au, Ag, TiN and ZrN nanoparticles on Si as a function of the laser fluence. The range for the nitrides corresponds to the exponent in Eq. (25) taking values between 1 and 1.3. The inset shows the Nd:YAG laser pulse profile (FWHM = 6 ns) assumed in the simulations.
makes it an important parameter in any SERS or surface-enhanced infrared absorption process.

4. Conclusions and outlook

The *ab initio* calculations reveal a qualitative common understanding for the optical properties of binary and ternary transition nitrides. The electronic conductivity of all these nitrides comes from the excess metal-d electrons that do not participate to the Metal-N bonding, which is the origin of the N-p → Metal-d interband transitions and of the accompanying dielectric losses. Quantitative variations do exist among the various nitrides, with the major trends being the increase of conduction electron density and the substantial blueshift of the interband transitions with increasing the number of valence electrons of the constituent metal. However, relying exclusively to *ab initio* calculations, which assume an ideal, defect-free nitride crystal in the B1 cubic structure, might be misleading. This is because of the metastable nature of some B1 nitrides (e.g. B1-TaN) and the intrinsic point defects, which are necessary to stabilize the B1 structure (e.g. B1-MoN and B1-WN). Even for the cases where the B1 structure is stable (such as B1-TiN, B1-ZrN and B1-NbN) kinetic and thermodynamic factors can severely affect the crystal growth process altering, or even opposing, the predictions of the *ab initio* calculations regarding the optical and plasmonic properties of these nitrides.

The critical comparison of the experimental optical spectra undisputedly reveals that the less optically lossy nitrides are those of group IVb metals (TiN, ZrN, HfN). Among them, ZrN shows the longest average value electron relaxation time, combined with the minimized dielectric losses, and it is emerging as the most promising refractory conductor for plasmonics. In addition, TiN and ZrN exhibit small and large work function, respectively, while they have similar melting points and conduction electron densities. Therefore, they and their alloys can constitute a platform of plasmonic conductors of tunable work function for hot electron applications. TiN by itself (i.e. without alloying) can be quite tunable, while ZrN is less tunable but it can be superior in its short range of operation by providing shorter SPP wavelengths due to the less dielectric losses. The LSPR performance of TiN is as strong as that of gold albeit with broader resonances, and manifests at exactly the same spectral range with gold. ZrN exhibits LSPR that is spectrally in between of gold and silver, and the strength of the resonance is intermediate between gold and silver as well. HfN exhibits intermediate optical performance and cell size, and given its scarcity and high cost seems to be less appealing for plasmonic applications.

Regarding the nitrides of Vb metals, they exhibit higher conduction electron density compared to group IVb nitrides, and thus a plasmonic performance towards UV is predicted. Given the metastable character of B1-TaN in contrast to the ease of fabricating epitaxial B1-NbN, we can safely conclude that for UV plasmonic applications B1-NbN is the most promising candidate. B1-VN received less attention and in this review only data from one sample are reported. These data indicate that B1-VN is not inferior to B1-NbN, while having the additional asset of exceptionally low work function. The combination of the potential plasmonic response in the UV with the low work function of B1-VN might be a strong incentive for the investigation of B1-VN in plasmonics and hot electron applications; however, its real potential for such applications cannot be solidly evaluated for the time being due to the lack of data. B1-TaN has quite acceptable optical and plasmonic response, but its growth without a high concentration of structural defects or the existence of a secondary phase is quite rare.

Finally, B1-MoN and B1-WN are exceptionally and excessively lossy due to both their inherent characteristics, and their metastable character, which results in the incorporation of a high concentration of point defects to stabilize them. Consequently, they do not seem appropriate for applications, such as plasmonics, where high conductivity is required.

All conductive transition metal nitrides exhibit very short intrinsic conduction electron mean free paths; consequently, their spectral tunability by varying the size and/or the shape of nanostructures is quite limited. This limitation can be overcome by the introduction of ternary conductive nitrides of varying conduction electron density. TiN-based alloyed ternary nitrides were found to outperform the ZrN-based ternaries, despite of the superior character of pure ZrN on its own merit. This is attributed to the very large mismatch or ZrN compared to the rest of the transition metal nitrides, which may cause the formation of extended structural defects that reduce the conductivity, as well as to the kinetically-hindered growth of Zr-containing nitride crystals. By evaluating and comparing an immense range of ternary combinations, we conclude that the most promising candidates based both on technical merit and on the abundance of the constituent elements, are Ti$_x$Ta$_{1-x}$N, Ti$_x$Zr$_{1-x}$N, Ti$_x$Sc$_{1-x}$N, Ti$_x$Al$_{1-x}$N, and Ti$_x$Mg$_{1-x}$N in the B1 rocksalt structure. They share the important plasmonic features with their binary counterparts, while having the additional asset of the exceptional spectral tunability in the entire visible (400–700 nm) Near Infrared (NIR, 700–1350 nm) and UVA (315–400 nm) spectral ranges depending on their net valence electrons per unit cell; thus, Ti$_x$Ta$_{1-x}$N is recommended for plasmonic devices in blue, violet and UV, Ti$_x$Zr$_{1-x}$N for red, and Ti$_x$Sc$_{1-x}$N and Ti$_x$Mg$_{1-x}$N for NIR. Especially, Ta-rich Ti$_x$Ta$_{1-x}$N outperforms the binary B1-TaN (and even the binary B1-NbN with the current state-of-the art, however, the comparison to B1-NbN cannot be conclusive due to the lack of optical spectra of epixtalial B1-NbN) for plasmonics: it seems that the incorporation of a small Ti content into TaN stabilizes the cubic B1 structure with beneficial results to the optical and plasmonic performance.

We have shown that nanoparticles of such ternary nitrides can exhibit maximum field enhancement factors inferior but comparable with gold in the aforementioned broadband range (315–1350 nm). These nitrides exhibit substantial electronic losses mostly due to fine crystalline grains that deteriorate the plasmonic field enhancement unequivocally calling for the improvement of the current crystal growth technology for these materials.

Finally, the transition metal nitrides are remarkably stable up to very high temperatures, due to their refractory character, and thus can endure the interactions with strong electric fields, such as in lasers. This opens new possibilities such as finely tuning the nanoparticle temperature up to very high values making it an important parameter of the plasmonic response, e.g. by inducing to the nitride nanoparticles a thermal bath into the energy range of most molecule vibrational modes affecting the SERS or surface-enhanced infrared absorption processes.

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