The Latest Method for Surface Tension Determination: Experimental Validation

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Abstract: The highest effectiveness of heat exchange is under boiling; hence, surface tension is an important parameter and should be determined when new liquid substances are created. The most popular methods are based on numerically solving the Young–Laplace equation by applying the Bashforth and Adams algorithm, which fails at the poles and at the inflection points. The newest algorithm is based on the closed-form expressions that define a drop or bubble. It gives the accurate solutions for the fully created drops or bubbles. To validate it, the surface tension value is determined for the air bubbles in water and compared with the reference data. Because the relative discrepancies are extremely small, the new method may be thought of as positively validated.

Keywords: surface tension; Young–Laplace equation; boiling; heat or mass transfer

1. Introduction

A necessity to increasing the effectiveness of energy transfer results in heat exchange under boiling conditions [1]. Hence, heat transfers across a free surface, which means that surface tension must be included into an analysis. Since new created substances take part in energy transfer, they thermodynamic properties, including surface tension, must be determined. In addition, surface tension is one of the parameters that determine the combustion efficiency [2–5]. It is also an important property of the new synthesized surfactants that are applied during the fuel processing [6,7]. Moreover, surface tension impacts on the hydraulic characteristics of transporting equipment [8]. Since clouds contain extremely small the water drops and ice particles, the surface effects should be taken into consideration [9–12]. In the last case, research is conducted for supercooled water [13].

The majority of commonly used methods for determining surface tension originate from an equation that was described by Young [14] and derived by Laplace (1806) (cf. Adamson [15])

$$\Delta p = \gamma \left(\frac{1}{R_1} + \frac{1}{R_2}\right),$$  (1)

where:

- $\Delta p$ - pressure difference between two sides of interface in the bulk phases [Pa];
- $\gamma$ - surface tension [N/m];
- $R_1$, $R_2$ - the main radii of curvature [m] (cf. Figure 1).
Although the ultimate cameras containing charge-coupled devices (CCD) are capable to capture the drop even at the apex of its creation and even after the creation. Moreover, these functions are continuously differentiable.

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Figure 1. Definitions of the variables in the Bashforth and Adams [16] algorithm. The location of a curvature center for the first radius $R_1$ is illustrative, and the center may be located in any point along the normal of the arc $ds$.

Since Young–Laplace Equation (1) does not contain any coordinate of an interface shape, Bashforth and Adams [16] proposed a numerical algorithm for its solution. The algorithm, which possesses numerous modifications (e.g., [17–27]), is a Cauchy problem and is applied to determining either an interface shape or surface tension value.

However, the algorithm fails when surface tension is determined from a spherical drop (e.g., at 24 °C $\gamma = 79.32 \pm 0.19$ N/m instead of 72.28 N/m), which was thoroughly investigated by Hoorfar and Neumann [28]. As a result of the comprehensive study, Hoorfar and Neumann [28] summarized that the algorithm has an intrinsic problem that cannot be surmounted by the numerical schemes improvements.

What is more, there is another insufficiency that is not discussed whatsoever. This insufficiency consists in the lack of a solution at a sharpened tip and tapering neighborhood. Thus, the algorithm is used only to solve pendant drops, and the solutions for the fully created droplets are not presented. For instance, the treatise on surface tension phenomena by Hartland and Hartley [17] does not show the solutions in the full range from 0° to 180°, in other words, there is no solution at the tapered apex. In addition, there is no chapter on the fully created drops or bubbles. For example, the shapes of the pendant interface are listed from $\Theta = 10^\circ$ to 179.064° and from $\Theta = 179.064^\circ$ to 0.935678° (cf. on page 170 in Hartland and Hartley [17]) or from $\Theta = 1^\circ$ to 6.36988° and from $\Theta = 6.36988^\circ$ to 0° (cf. on page 243 in Hartland and Hartley [17]). A lack of solution for $\Theta = 0^\circ$ that is at the most distant place from the nozzle should be emphasized. Undoubtedly, this is a place where the two-phase static model assumptions are satisfied in the experimental conditions most.

The Young–Laplace equation is the static two-phase model; hence, the experiment should satisfy these assumptions. Thus, the best experimental approximation is the state when the drop has just been disconnected from the nozzle (i.e., the third solid phase) and there is no flows inside or outside the drop. Although the ultimate cameras containing charge-coupled devices (CCD) are capable to capture the drop at such a moment, the Young–Laplace equation may not be solved at the poles of the drop.
2. Contemporary Interface Model

Nevertheless, there are the analytical functions that circumscribe either a drop or bubble under static conditions in the full range from 0° to 180°. Thus, a drop or bubble may be plotted in any phase of its creation and even after the creation. Moreover, these functions are continuously differentiable even at the apex, where the derivative of radial distance with respect to polar angle is 0 (cf. Gajewski [29,30]). Since, there are three variables that must be determined to obtain either surface tension or interfacial tension, the set of three equations must be solved. The unknowns are hydraulic head at the origin \( H \), square capillary constant \( a^2 \) and the cosine of polar angle \( \cos \theta_{\text{max}} \) for the minimal diameter. Forasmuch as there are investigated bubbles, the set of equations is as follows (cf. Gajewski [31]):

\[
d_{\text{max}} = \left( H + \left( H^2 - 8a^2 \cos \theta_{\text{max}} \right)^{\frac{1}{2}} \right) \tan \theta_{\text{max}} \tag{2}
\]

\[
h_{\text{max}} = \frac{1}{2} \left( + \left( H^2 - 8a^2 \cos \theta_{\text{max}} \right)^{\frac{1}{2}} - \left( H^2 + 8a^2 \right)^{\frac{1}{2}} \right) \tag{3}
\]

\[
0 = H^2 + H \left( H^2 - 8a^2 \cos \theta_{\text{max}} \right)^{\frac{1}{2}} - 4a^2 \cos \theta_{\text{max}} \left( 1 + \cos^2 \theta_{\text{max}} \right), \tag{4}
\]

where:

- \( H \) - hydraulic head at the origin [m];
- \( d_{\text{max}} \) [m], \( h_{\text{max}} \) [m], and \( \theta_{\text{max}} \) are the sizes at the widest diameter of the bubble (cf. Figure 2), and they are negative numbers in the case of the bubbles;

\[\text{Figure 2.} \text{ Shape of a bubble at creation if the ratio of the hydraulic head and capillary constant equals the square root of 8. The inner part contains a lighter gas, while the surroundings is a denser liquid, } r_{\text{max}} \text{ and } \theta_{\text{max}} \text{ are the spherical coordinates at the widest diameter of the bubble.}\]
\(a^2\)- square capillary constant \([\text{m}^2]\) is defined beneath.

\[
a^2 = \frac{\gamma'}{(\rho_{dl} - \rho_{lf})g},
\]

where:
- \(g\) - gravitational acceleration \([\text{m/s}^2]\);
- \(\gamma\) - surface tension \([\text{N/m}]\);
- \(\rho_{dl}\) – density of denser liquid \([\text{kg/m}^3]\);
- \(\rho_{lf}\) – density of lighter fluid \([\text{kg/m}^3]\).

The sizes \(d_{max}\) and \(h_{max}\) are measured in a photograph, while \(a^2\), \(H\), and \(\cos \theta_{max}\) are the unknowns, which are the solutions of Equations (2)–(4).

The capillary constant definition contains the density difference of a denser liquid and lighter fluid. In fact, the computations are done in a vector space. Consequently, a surface vector is pointed from the denser liquid into the lighter fluid. In the case of a drop of the denser liquid, a normal unit vector is collinear with the surface vector. As a result, we obtain positive values of radial distance \(r\), polar angle \(\theta\), and hydraulic head \(H\) at the origin. In the case of a bubble or lighter drop, the senses of the normal unit vector and the proper surface vector are in the opposite directions. For this reason, a solution of the force balance yields the negative coordinate of a radius \(r\) that is pointed from the denser liquid to the lighter fluid. Moreover, zenith angle \(\theta\) is measured anticlockwise (cf. Figure 2), hence its value is negative. Thus, other quantities, such as a diameter \(d\), height \(h\), or hydraulic head \(H\) have to be the negative numbers.

Gajewski [31] decomposed Equations (2)–(4), which yielded two systems of equation as the solutions. The first set of the equations is solved in the consecutive iterations.

\[
\cos \theta_{max} = 1 - \frac{h_{max}}{2a^2} \left[ h_{max} + \left( \frac{H^2 + 8a^2}{1 - \cos^2 \theta_{max}} \right)^{\frac{1}{2}} \right],
\]

\[
H = d_{max} \frac{\cos \theta_{max}}{\left( 1 - \cos^2 \theta_{max} \right)^{\frac{1}{2}}} + \frac{4a^2}{d_{max}} \left( 1 - \cos^2 \theta_{max} \right)^{\frac{3}{2}},
\]

\[
a^2 = \frac{d_{max}}{8(1 - \cos^2 \theta_{max})} \left[ 2H \left( 1 - \cos^2 \theta_{max} \right)^{\frac{1}{2}} - d_{max} \cos \theta_{max} \right],
\]  

The second system consists of four equations in which only Equation (9) is solved by iterating (cf. Gajewski [31]).

\[
4h_{max}^2 \cos \theta_{max} (1 - \cos \theta_{max}) + 2h_{max} d_{max} (1 - \cos \theta_{max}) \left( 1 - \cos^2 \theta_{max} \right)^{\frac{1}{2}} = 0,
\]

\[
a' = -\frac{d_{max}}{2(2\cos \theta_{max} (1 - \cos^2 \theta_{max}))^{\frac{1}{2}}},
\]

\[
a = -\frac{h_{max} (2\cos \theta_{max})^{\frac{1}{2}}}{\left[ (1 + \cos^2 \theta_{max})^2 + 4\cos \theta_{max} \right]^{\frac{1}{2}} - 1 + \cos^2 \theta_{max}},
\]

\[
H = -a \left( 1 + \cos^2 \theta_{max} \right) \left( \frac{2}{\cos \theta_{max}} \right)^{\frac{1}{2}}.
\]

The aim of the investigations is a validation of the latest method with the air–water surface tension values as the reference.
3. The Experiment

The experiment is conducted using the system of apparatus described hereinafter. Air compressor (1a in Figure 3) supplies air to the plenum tank (1b) from which air flows through a tube (1) in Figure 4 and temperature equalizer (2) to the nozzle (3). The water is heated by an electric heater (4), water temperature is measured with a thermocouple type K (5) and recorded with a testo-435 gauge (which is out of the photograph). Dry- and wet-bulb air temperature ($T_d$ and $T_w$, respectively) as well as air pressure are measured with an indoor air quality (IAQ) probe (6), which is connected with the testo-435 gauge. The image of a bubble is captured by a CCD camera (which is out of the photograph) and is screened in the monitor (7).

Figure 3. Air compressor (1a) and the plenum tank (1b).
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Figure 3. Air compressor (1a) and the plenum tank (1b).

Figure 4. Applied system of apparatus: 1—a tube supplied air, 2—temperature equalizer, 3—nozzle, 4—electric heater, 5—thermocouple, 6—IAQ probe, 7—monitor with a creating bubble.

4. Determining Specific Gravity of the Fluids

Specific gravity is a product of density and gravitational acceleration that is obtained from Nawrot et. al’s [32] formula.

$$g = 9.780318\left(1 + 0.0053024\sin^2\varphi - 0.000058\sin^22\varphi\right) - 0.000003086z \text{ [m/s}^2\text{]}, \quad (13)$$

where $\varphi$ is latitude, and $z$ is altitude in meters above mean sea level. After a substitution of $\varphi$ and $z$ for the system of apparatus, the gravitational acceleration at the laboratory is 9.81295907 m/s$^2$.

Fluid Densities Determination

The water density values are taken from Çengel and Cimbala [33]. To obtain moist air density, the specific humidity of air $x$ [-] must be determined, which is done by using the following formula (cf. Çengel and Boles [34] or Ferencowicz [35]):

$$x = \frac{\varphi p_{sat}}{p_{air} - \varphi p_{sat}}, \quad (14)$$

where:

- $p_{air}$ - absolute air pressure [Pa];
- $p_{sat}$ - saturation pressure of water at dry-bulb temperature [Pa];
- $R_{air}$ - specific gas constant for dry air [J/(kg·K)];
- $R_v$ - specific gas constant for water vapor [J/(kg·K)];
- $\varphi$ - relative humidity [-].

Ferencowicz [35] derived a following relation for moist air density $\rho_{air}$ [kg/m$^3$]:

$$\rho_{air} = \frac{p_{air}(1 + x)}{T_d(R_{air} + xR_v)}, \quad (15)$$

where:
$T_d$ – dry-bulb temperature [K].

Since air density is relatively small compared to water density, the relative humidity is taken from the gauge. Thus, it is substituted for $x$ in Equation (15) with Equation (14) and we obtain moist air density as the function:

$$\rho_{air} = \frac{p_{air} + \varphi p_{sat}(\frac{R_{air}}{R_v} - 1)}{T_d R_{air}}. \quad (16)$$

5. Results and Discussion

After each experiment, the diameters $d_{max}$ and heights $h_{max}$ are measured in the photographs, the illustrative measurements are attached in Supplementary Materials. The measured dimensions in the experiment are written down in Table 1. Then, either Equations (6)–(8) or the Equations (9)–(12) are solved.

| Point Number | $t$ [°C] | $d_{max}$ [mm] | $h_{max}$ [mm] |
|--------------|----------|----------------|----------------|
| 1            | 1.20     | -4.076         | -2.256         |
| 2            | 5.10     | -4.062         | -2.248         |
| 3            | 9.90     | -4.043         | -2.238         |
| 4            | 15.20    | -4.024         | -2.227         |
| 5            | 20.10    | -4.005         | -2.217         |

When capillary constant $a$ is obtained from either of Equations (8), (10), or (11) and specific weights of both fluids are known, the surface tension value may be determined from Equation (5). The solution is done in a spreadsheet which is attached in Supplementary Materials. Figure 5 shows the final results. There are also plotted two reference surface tension values Çengel and Cimbala [33] as well as The International Association for the Properties of Water and Steam (IAPWS) [36] experimental data, which both are used as the benchmark values to validating the experimental results.

![Figure 5](image-url)  

**Figure 5.** Results obtained from Equation (5) and the reference data from Çengel and Cimbala [33] and IAPWS [36]. The relative discrepancies between the Çengel and Cimbala [33] reference data and the experimental results are presented in the labels.
The models based on the Bashforth and Adams [16] approach require both considerable research experience and an advanced application program. Otherwise, the obtained surface tension values might be improper. Contrastively, the new method requires only thoroughness.

6. Conclusions

The relative discrepancies between the surface tension value obtained from the newest method and the reliable data are relatively small. Therefore, it may be concluded that the newest method for surface tension determination is positively validated.

Supplementary Materials: The following are available online at http://www.mdpi.com/1996-1073/13/14/3629/s1, Figure S1: A still at 5 °C, Figure S2: A still at 15 °C, Spreadsheet “Surface tension determination for water-air interface.xlsx.”

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