A “Baedecker” for the Dark Matter Annihilation Signal

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We provide a “Baedecker” or travel guide to the directions on the sky where the dark matter annihilation signal may be expected. We calculate the flux of high energy γ-rays from annihilation of neutralino dark matter in the centre of the Milky Way and the three nearest dwarf spheroidals (Sagittarius, Draco and Canis Major), using realistic models of the dark matter distribution. Other investigators have used cusped dark halo profiles (such as the Navarro-Frenk-White) to claim a significant signal. This ignores the substantial astrophysical evidence that the Milky Way is not dark-matter dominated in the inner regions. We show that the annihilation signal from the Galactic Centre falls by two orders of magnitude on substituting a cored dark matter density profile for a cusped one. The present and future generation of high energy γ-ray detectors, whether atmospheric Cerenkov telescopes or space missions like GLAST, lack the sensitivity to detect any of the monochromatic γ-ray annihilation lines. The continuum γ-ray signal above 1 GeV and above 50 GeV may however be detectable either from the dwarf spheroidals or from the Milky Way itself. If the density profiles of the dwarf spheroidals are cusped, then the best prospects are for detecting Sagittarius and Canis Major. However, if the dwarf spheroidals have milder, cored profiles, then the annihilation signal is not detectable. For GLAST, an attractive strategy is to exploit the wide field of view and observe the Milky Way at medium latitudes, as suggested by Stoehr et al. This is reasonably robust against changes in the density profile.

I. INTRODUCTION

The foremost candidate for the cold dark matter (CDM) composing galactic haloes is the lightest neutral supersymmetric particle, namely the neutralino. If so, then neutralino pair annihilation may lead to observable consequences, in particular the emission of high energy γ-radiation. The possibility that such γ-rays may be identified by forthcoming atmospheric Cerenkov telescopes (ACT) such as VERITAS or by satellite-borne detectors like GLAST has excited considerable recent interest.

It is clearly of importance to identify the best places to search for such an annihilation signal. Inspired by the highly cusped models based on numerical simulations of dark halo formation, a number of investigators have suggested that the centre of the Milky Way may be the optimum target. For example, Bergstrom et al. have shown that if the dark matter density is cusped as 1/r at small radii, then the γ-ray flux would be detectable for typical neutralino properties in the minimal supersymmetric extension of the Standard Model. Inspired also by the persistence of substructure in numerical simulations, a number of authors have argued that a substantial enhancement in the γ-ray signal can be expected from such ‘clumps’. In these calculations, the inner regions of the substructure are also usually assumed to be cusped. However, even within the framework of the cusped models favored by cosmological simulations, these conclusions have been contested as being overly optimistic.

More awkwardly, there is a substantial body of astrophysical evidence that the halo of the Milky Way is not cusped at all. First, the microlensing optical depth towards the Galactic Center is very high. Particle dark matter does not cause microlensing, whereas faint stars and brown dwarfs do. The total amount of all matter within the Solar circle is constrained by the rotation curve, so this tells us that lines of sight towards the Galactic Center are not dominated by particle dark matter. More specifically, haloes as strongly cusped as 1/r, normalised to the local dark matter density as inferred from the stellar kinematics in the solar neighbourhood, are ruled out by the high microlensing optical depth. Second, the pattern speed of the Galactic bar is known to be fast from hydrodynamical modelling of the motions of neutral and ionised gas. If dark matter dominates the central regions of the Milky Way, then dynamical friction will strongly couple the dark matter to the Galactic bar and cause it to decelerate on a few bar rotation timescales. It is now largely accepted by astronomers that bright galaxies like the Milky Way do not have cusped dark haloes today, with some investigators suggesting that feedback from star formation may provide a resolution with cold dark matter theories.

In fact, there is no observational evidence whatsoever that any nearby galaxy has a cusped dark halo profile. The rotation curves of low surface brightness and dwarf spiral galaxies have been the subject of a long controversy. The effects of beam smearing mean that the HI rotation curves of many dwarf spirals are broadly compatible with both cores and cusps. However, the HII rotation curves for at least some dwarf spirals are not compatible with cusps. Most dwarf spheroidals (dSphs) do not contain gas and so the structure of the dark halos must be inferred from stellar motions. Very recently, the survival of kinematically cold substructure in the Ursa Minor dSph has been used to argue against a cusped halo. Hence, even at the least massive and most dark matter dominated end of the
Dwarf spheroidals (dSphs) warrant attention because they are amongst the most extreme dark matter dominated environments. For example, the mass-to-light ratio of Draco is \( \sim 250 \) in Solar units \[21\], while that of the Sagittarius is \( \sim 100 \) \[22\]. The recently discovered possible dSph in Canis Major seems similar to the Sagittarius in structural properties and dark matter content \[23\]. Given the seeming absence of dark matter in globular clusters, dSphs are also the smallest systems dominated by dark matter.

We develop two sets of models of dSphs. The first set is the cored spherical power-law models \[24\]:

\[
\rho_{\text{pow}}(r) = \frac{\rho_0}{r^\alpha(1 + \frac{r}{r_0})^{3-\alpha/2}}.
\]

Here, \( r_0 \) is the core radius and \( \rho_0 \) is a velocity scale. When \( \alpha = 0 \), the model has an asymptotically flat rotation curve and is the cored isothermal sphere. The rotation curves of dwarf galaxies may be gently rising or falling at large radii, so we also consider models with \( \alpha = -0.2 \) and 0.2 respectively.

The second set of models is the cusped haloes

\[
\rho_{\text{cusp}}(r) = \frac{A}{r^\gamma(r + r_s)^3-\gamma},
\]

favored by numerical simulations. Here, \( r_s \) is the scale radius and \( A \) is the overall normalisation. When \( \gamma = 1.5 \), the model is the highly cusped Moore et al. \[10\] profile, when \( \gamma = 1 \), the model is the Navarro-Frenk-White (NFW) profile \[25\]. Additionally, we study the case \( \gamma = 0.5 \) which represents a still milder cusped profile.

The two free parameters determining the shape of the profile are set by fitting to observational data on the Draco dSph using the Jeans equation \[24\]. For a spherical galaxy, the enclosed mass \( M(r) \) is related to observables via

\[
M(r) = -\frac{r\langle v_r^2 \rangle^2}{G} \left( \frac{d \log \nu}{d \log r} + \frac{d \log \langle v_r^2 \rangle}{d \log r} + 2\beta \right).
\]

Here, \( \nu \) is the luminosity density, \( \langle v_r^2 \rangle \) is the radial velocity dispersion of the stars and \( \beta \) is the anisotropy of the stellar motions. The luminosity density of Draco \( \nu \) is taken as \[22\]:

\[
\nu = \frac{\nu_0 r_0^5}{(r_0^2 + r^2)^{3/2}},
\]

with \( r_0 = 9.71' \approx 0.23 \) kpc (using a heliocentric distance for Draco of 82 kpc). There are 6 observational points showing the line of sight velocity dispersion of Draco at different radii in \[27\] (using the data with no rotation subtracted). The datapoints are consistent with a flat profile between \( 2' \) and \( 22' \). Assuming that the anisotropy now vanishes, then the radial velocity dispersion is equal to the line-of-sight velocity dispersion. Finally, the left-hand side of eq. \[3\] is fitted to the known right-hand side at the locations of the datapoints in \[27\], thus giving estimates for the two unknown parameters for each density profile as quoted in Table \[1\].

This algorithm provides models of the Draco dSph that satisfy the available observational data. Unfortunately, the radial variation of the velocity dispersion has not been measured for the Sagittarius dSph. However, the central line-of-sight velocity dispersion of Sagittarius dSph is \( 11.4 \) kms\(^{-1}\), very similar to that of Draco (10 kms\(^{-1}\)). Henceforth, we assume that the underlying structural parameters \( (r_s, r_0) \) or \( A, r_s \) of the Sagittarius dSph are the same as Draco. The third dSph under study – Canis Major – has only recently been claimed and the evidence for its existence is not yet clear-cut. There is certainly a surprising concentration of stars in the direction of Canis Major, but this could...
Cored Power-Law Models

| $\alpha$ | $\nu_a$ km s$^{-1}$ | $r_c$ kpc | $r_t$ kpc | $M(r_t) \div 10^8 M_\odot$ |
|----------|---------------------|------------|------------|-----------------|
| 0.2      | 24.7                | 0.25       | 6.2 (2.16) | 1.3 (0.5)       | 4.6 (2.0)      |
| 0        | 22.9                | 0.23       | 7.8 (2.5)  | 1.4 (0.51)      | 9.5 (3.0)      |
| -0.2     | 20.9                | 0.21       | 10.1 (2.8) | 1.6 (0.52)      | 22.43 (4.9)    |

MW - Iso | MW - NFW

Cusped Models

| $\gamma$ | $A \times 10^7 M_\odot$ | $r_s$ kpc | $r_c$ kpc | $r_t$ kpc | $M(r_t) \div 10^8 M_\odot$ |
|----------|--------------------------|------------|------------|------------|-----------------|
| 0.5      | 2.3                      | 0.32       | 6.6 (2.5)  | 1.5 (0.6)  | 5.5 (3.1)      |
| 1 (NFW)  | 3.3                      | 0.62       | 7.0 (2.59) | 1.6 (0.57) | 6.6 (3.5)      |
| 1.5 (Moore) | 2.9                    | 1.0        | 6.5 (2.4)  | 1.5 (0.6)  | 5.5 (2.8)      |

MW - Iso | MW - NFW

TABLE I: Parameters of the dark matter halo profiles of the Draco dSph. The last three columns also give (in parentheses) the values at the location of the Sagittarius dSph. Two values are given for the tidal radius, according to whether the Milky Way halo is modelled with an isothermal power-law model or a NFW model. [Notes: (1) the models sometimes require a slight velocity anisotropy in the very innermost parts to ensure everywhere physical stresses in the Jeans equation, (2) the scale radius $r_s$ is constrained to lie below 1 kpc].

To determine the extent of the dark matter halo of the dSphs, the tidal radius must be estimated. The approximate method used conventionally is derived from the Roche criterion. The tidal radius is found by requiring that the average mass in the dSph is equal to the average interior mass in the Milky Way halo, namely

$$\frac{M_{dSph}(r_t)}{r_t^3} = \frac{M_{MW}(r_{dSph} - r_t)}{(r_{dSph} - r_t)^3}.$$  (5)

Here, $M_{MW}(r)$ and $M_{dSph}(r)$ are the masses enclosed within radius $r$ of the Milky Way halo and the dwarf spheroidal respectively, while $r_{dSph}$ is the distance from the Galactic Center to the centre of the dSph. We remark that this is not the same as the procedure used in a number of recent papers [28, 29], in which the local density at the tidal radius in the dSph is set equal to the density of the background Milky Way halo at the center of the dSph.

The results depend on the choice of profile for the Milky Way halo. For comparison purposes, we consider both a cored isothermal profile with $r_c = 10$ kpc and $\nu_a = 220$ kms$^{-1}$, and a NFW profile with concentration parameter $c = 10$. The total mass of the Milky Way halo is fixed at $M_{MW} \sim 10^{12} M_\odot$, as suggested in [30]. We show in Table I the results when eq. (5) is used to determine the tidal radius of a dSph at the locations of Draco and Sagittarius, for the two adopted models of the Milky Way halo.

### III. THE GAMMA-RAY FLUX

Let the neutralino mass be $m_\chi$ and its self-annihilation cross-section be $\langle \sigma v \rangle$. Then, the $\gamma$-ray flux from neutralino annihilation is given by [2]

$$\Phi_\gamma(\psi) = \frac{N_\gamma \langle \sigma v \rangle}{4 \pi m_\chi^2} \times \frac{1}{\Delta \Omega} \int d\Omega \int_{\text{los}} \rho^2[r(s)] ds,$$  (6)

where $\rho$ is the density of the dSph as a function of distance from its center $r$, which of course depends on the heliocentric distance $s$. The integration is performed along the line-of-sight to the target and averaged over the solid angle $\Delta \Omega$ of the detector. In particular, $N_\gamma = 2$ for the annihilation of two non-relativistic neutralinos into two photons ($\chi \bar{\chi} \rightarrow \gamma \gamma$) and $N_\gamma = 1$ for the annihilation into a photon and a Z boson ($\chi \bar{\chi} \rightarrow Z \gamma$). The first part of the integrand (6) depends on the particular particle physics model for neutralino annihilations. The second part is a line-of-sight integration through the dark matter density distribution. We discuss each in detail in the next two subsections.
mSUGRA parameters

| $m_0$ (GeV) | $m_{1/2}$ (GeV) | $\tan \beta$ | $|A_0|$ (GeV) |
|------------|----------------|-------------|-------------|
| 10-10000   | 10-10000       | 1-60        | 10-10000    |

TABLE II: The portion of the mSUGRA parameter space randomly scanned to generate the models. Here, $m_0$ and $m_{1/2}$ are respectively the common scalar and gaugino mass at the unification scale, while $A_0$ is the trilinear parameter and $\tan \beta$ is the ratio of the vacuum expectation values of the two Higgs fields. The $\mu$ term in the Lagrangian is allowed to have either sign.

A. Particle Physics Model

To compute $N_\chi \langle \sigma v \rangle/(4\pi m^2_\chi)$, we have to select a supersymmetric model. We focus on minimal supergravity (mSUGRA) models with universal gaugino and scalar masses and trilinear terms at the unification scale $\tilde{M}$. We use the computer programme SoftSusy [32] to scan the supersymmetric parameter space (see Table III) and generate $10^5$ models which have consistent electroweak symmetry breaking and grand unification. The output at the electroweak scale is fed into the programme DarkSusy [33] which computes the relic density and products of the neutralino annihilations. It also checks that a given model is not ruled out by present accelerator experiments.

A feasible model is one which is permitted by accelerator limits and which predicts a relic density in the range $0.005 < \Omega_{\text{CDM}} h^2 < 0.2$. This is somewhat broader than the range $0.09 < \Omega_{\text{CDM}} h^2 < 0.13$ determined by fitting the standard $\Lambda$CDM model to the WMAP data [34]. This is done so as to incorporate the higher values for $\Omega_{\text{CDM}} h^2$ found for consistent alternative CDM models [35]. The lower limit is set by requiring the relic particle to provide most of the dark matter in galaxies (taking a typical mass-to-light ratio for galaxies of $\sim 10$, cf. the critical mass to light ratio of $\sim 2000$ in solar units). The range of the supersymmetric parameters scanned are given in Table II. For each feasible model, we record the quantities $N_\chi \langle \sigma v \rangle$ for the discrete lines $\chi\chi \rightarrow \gamma\gamma$ and $\chi\chi \rightarrow Z\gamma$, as well as the continuous $\gamma$-ray spectrum above 1 and 50 GeV. Note that in the previous study [2], the relic density was much less constrained and models with an arbitrary low values were permitted.

B. Line-of-Sight Integration of Dark Matter Density

The line-of-sight integration can be manipulated thus:

$$\langle J \rangle_{\Delta \Omega} = \frac{1}{\Delta \Omega} \int_{\Delta \Omega} J(\psi)d\Omega = \frac{2\pi}{\Delta \Omega} \int_0^{\theta_{\max}} d\theta \sin \theta \int_{s_{\min}}^{s_{\max}} ds \rho^2 \left( \sqrt{s^2 + s_0^2 - 2ss_0 \cos \theta} \right)$$

where

$$J(\psi) = \int \rho^2(r)ds$$

In these formulae, angled brackets denote the averaging over the solid angle $\Delta \Omega$, while $s_{\min}$ and $s_{\max}$ are the lower and upper limits of the line-of-sight integration, given by $s_0 \cos \theta \pm \sqrt{r_t^2 - s_0^2 \sin^2 \theta}$. Here, $s_0$ is the heliocentric distance of the dSph and $r_t$ is the tidal radius of the dSph. Finally, $\theta_{\max}$ is the angle over which we average around the center of the dSph. It generally is, at least, equal to the experimental resolution and can be fixed using:

$$\Delta \Omega = 2\pi \int_0^{\theta_{\max}} d\theta \sin \theta = 2\pi (1 - \cos(\theta_{\max})).$$

The quoted point spread function widths for the various experiments are: $0.4^\circ$ (EGRET), $0.1^\circ$ (GLAST, HESS and VERITAS), $0.15^\circ$ - $0.04^\circ$ (CANGAROO-III). EGRET and GLAST are satellite detectors with low energy thresholds ($\approx 100$ MeV), high energy resolution ($\approx 15\%$) but only moderate angular precision. The others are ACTs with higher thresholds ($\approx 100$ GeV) but better angular resolution. Typical reference sizes for the solid angle are $\Delta \Omega = 10^{-5}$ sr for ACTs and GLAST and $\Delta \Omega = 10^{-3}$ sr for EGRET.

Table III lists values of $\langle J \rangle_{\Delta \Omega}$ for the dSph profiles introduced in Section II. The heliocentric distances to the Draco, Sagittarius and Canis Major dSphs are $\sim 80, 24$ and $8$ kpc respectively and this largely controls the relative values of $\langle J \rangle_{\Delta \Omega}$ for the three dSphs. Clearly, the comparative closeness of the Canis Major dSph works to its advantage as a possible target. An increase in angular sensitivity enhances the signal for all three dSphs. We remark that, in the literature, there is a considerable spread in the values obtained for $\langle J \rangle_{\Delta \Omega}$ for different sources. In [7], a 1-component
Cored Power-Law Models

\[
\alpha \\
\Delta \Omega = 10^{-3} \text{ sr} & \Delta \Omega = 10^{-5} \text{ sr} & \Delta \Omega = 10^{-3} \text{ sr} & \Delta \Omega = 10^{-5} \text{ sr} & \\
0.2 & 0.6 & 3.4 & 0.07 & 2.2 & 2.4 & 3.4 \\
0 & 0.6 & 3.3 & 0.06 & 2.2 & 2.4 & 3.5 \\
-0.2 & 0.6 & 3.2 & 0.07 & 2.2 & 2.4 & 3.4
\]

Cusped Models

\[
\gamma \\
\Delta \Omega = 10^{-3} \text{ sr} & \Delta \Omega = 10^{-5} \text{ sr} & \Delta \Omega = 10^{-3} \text{ sr} & \Delta \Omega = 10^{-5} \text{ sr} & \\
0.5 & 1.1 & 17.8 & 0.1 & 5.7 & 6.2 & 32.3 \\
1 \text{ (NFW)} & 1.3 & 3.6 & 0.1 & 7.2 & 8.3 & 139.9 \\
1.5 \text{ (Moore)} & 7.3 & 615.1 & 0.6 & 55.4 & 49.1 & 5469
\]

Galactic Center

\[
\text{Profile} & \Delta \Omega = 10^{-3} \text{ sr} & \Delta \Omega = 10^{-5} \text{ sr} \\
\text{NFW, } \gamma = 1 & 26 & 280 \\
\text{Cored, } \alpha = 0 & 0.3 & 0.3
\]

TABLE III: Values of \(\langle J \rangle_{\Delta \Omega}\) for the Sagittarius, Draco and Canis Major dSphs in units of \(10^{23} \text{ GeV}^2 \text{ cm}^{-5}\). The tidal radius of the dSphs is calculated assuming an isothermal profile for the Galactic halo. Additionally, results in the direction of the Galactic Center are given for both the NFW and isothermal models of the Galactic halo.

King profile was used to model the dSph density distribution. These authors only give explicit estimates of the entire line-of-sight integral. However, the values are of the order of \(10^{21} \text{ GeV}^2 \text{ cm}^{-5}\), lower than those implied by Table III. In [8], no angular average is taken, but instead the approximation

\[
J \approx \int_{\text{los}} \rho^2(l)dl \frac{4\pi d^2}{4\pi d^2},
\]

is used, together with an singular isothermal profile for Draco. Taking the value given for \(m_\chi = 100 \text{ GeV}\) implies \(3.7 \times 10^{20} \text{ GeV}^2 \text{ cm}^{-5}\) for the line-of-sight integral. It is surprisingly low and yet the plots manage to exclude as large a region in parameter space as in [2]! As we discuss in Section V, the reason for this is the criterion used in [8] to identify a detectable signal.

As seen in the bottom panel of Table III, the \(\gamma\)-ray emission towards the Galactic Center falls by at least two orders of magnitude on moving from a cusped NFW halo to a cored isothermal model. The point that the signal from the Galactic Center depends sensitively on the assumed halo profile, and so may have been overestimated, has also been made recently by Stoehr et al. [6]. For example, an optimistic result for the \(\gamma\)-ray flux towards the Galactic Center was obtained in [2] by using a cusped NFW model normalised to satisfy two constraints on the halo mass \(M\) and circular speed \(v_h\), namely

\[
M(r < 100 \text{ kpc}) = (6.3 \pm 2.5) \times 10^{11} M_\odot, \quad v_h(R_0) \approx 128 - 207 \text{ km s}^{-1}
\]

If the normalisation is set to obtain the maximum flux (as is done for example in Fig. 9 of [2]), then the models possess a local dark matter density substantially in excess of the usual value of \(\sim 0.3 \text{ GeV cm}^{-3}\). Anyhow, even accepting the debatable proposition that the Galaxy did once have a pristine dark halo of the NFW form, the formation of the Galactic disk, bulge and bar will have substantially re-processed the dark matter distribution. Certainly, the evidence from the microlensing optical depth towards the Galactic Centre and the pattern speed of the Galactic bar are inconsistent with models dominated by dark matter in the central regions [13].

Finally, let us illustrate how to convert the numbers in Table III into photon fluxes. This requires adopting characteristic values for the particle physics parameters; here, we take \(m_\chi = 100 \text{ GeV}\) and \(N_\gamma \langle \sigma v \rangle = 10^{-25} \text{ cm}^3 \text{ s}^{-1}\) for energies in excess of 1 GeV. Assuming the field of view is fixed at \(3^\circ\) (in other words, the semi-angle of the cone whose axis points towards the center of the objects is \(1.5^\circ\)), the implied photon fluxes from the Sagittarius, Draco and Canis Major dSphs are as given in Table IV.
IV. COMPUTATION OF THE BACKGROUND

There are three sources of background for the signal under consideration: hadronic, cosmic-ray electrons and diffuse $\gamma$-rays from astrophysical processes. The last is negligible for ACTs, but is the only one present for satellite experiments like GLAST or EGRET. Let us consider each source of background in turn.

A. Hadronic and Electronic

Bergstrom et. al. [2] use data taken with the Whipple ACT to derive the following expression for the hadronic background:

$$\frac{d\Phi_{\text{had}}}{d\Omega} (E > E_0) = 6.1 \times 10^{-3} \epsilon_{\text{had}} \left( \frac{E_0}{1 \text{ GeV}} \right)^{-1.7} \text{cm}^{-2}\text{s}^{-1}\text{sr}^{-1},$$

where $\epsilon_{\text{had}}$ is intended to take into account improved hadronic rejection expected in future ACTs, but is at present set to unity.

Showers initiated by cosmic-ray electrons are indistinguishable from gamma rays. This contribution to the background for ACTs is, according to [2] (who cite [36] for this purpose):

$$\frac{d\Phi_{\text{e}}}{d\Omega} = 3 \times 10^{-2} \left( \frac{E_0}{1 \text{ GeV}} \right)^{-2.3} \text{cm}^{-2}\text{s}^{-1}\text{sr}^{-1}.$$

B. Diffuse Emission

The diffuse $\gamma$-ray background is usually taken to be dominated by the Galactic [37] or extragalactic [38] contribution, depending on whether the target location is the Galactic Center or at higher latitudes ($b \geq 10^\circ$). For example, a fit to the EGRET data [37] at 1 GeV (dominated by the Galactic contribution) is given in [2] as

$$\frac{d\Phi_{\text{diff}}}{d\Omega dE} = N_0(l, b)10^{-6} \left( \frac{E_0}{1 \text{ GeV}} \right)^{-2.7} \text{cm}^{-2}\text{s}^{-1}\text{sr}^{-1}\text{GeV}^{-1},$$

where $N_0(l, b)$ is a factor in the range 1–100, with higher values for the central regions of the Galaxy. In [2], only the extragalactic contribution from EGRET, estimated in [38], is considered:

$$\frac{d\Phi_{\text{diff}}}{d\Omega dE} = (7.32 \pm 0.34) \times 10^{-9} \left( \frac{E_0}{451 \text{ MeV}} \right)^{-2.10 \pm 0.03} \text{cm}^{-2}\text{s}^{-1}\text{sr}^{-1}\text{MeV}^{-1}$$

$$\approx 1.4 \times 10^{-6} \left( \frac{E_0}{1 \text{ GeV}} \right)^{-2.10 \pm 0.03} \text{cm}^{-2}\text{s}^{-1}\text{sr}^{-1}\text{GeV}^{-1}. \quad (14)$$

So, the spectral indices of the Galactic and extragalactic contributions are about -2.7 and -2.1 respectively.

However, the separation between the Galactic and extragalactic background is not clear. For example in [39], the case is made for a very low extragalactic background. Studying the region around the Galactic poles ($b \approx 90^\circ$), it seems that, even there, most of the contribution is of Galactic origin. In particular, the main contribution is not.
isotropic but correlated with known Galactic tracers. The EGRET collaboration concede that any simple model for
the diffuse background is unlikely to work for all points in the sky and at all energies \[40\].

To be conservative, we normalize the flux to the EGRET data above 1 GeV and choose a spectral index of -2.1
which is the worst case:

\[
\frac{d\Phi_{\text{diff}}}{d\Omega dE} = N \left( \frac{E}{1 \text{ GeV}} \right)^{-2.1}.
\]

The emission above 1 GeV in the region of our interest can be downloaded from the EGRET website \[41\]. The exact
values for the diffuse emission are \(6.7 \times 10^{-7}\) cm\(^{-2}\) s\(^{-1}\) sr\(^{-1}\) at the location of the Draco dSph \((l = 86.4^\circ, b = 34.7^\circ)\),
\(3.18 \times 10^{-6}\) cm\(^{-2}\) s\(^{-1}\) sr\(^{-1}\) at the location of the Sagittarius dSph \((l = 5.6^\circ, b = -14.1^\circ)\), and \(1.2 \times 10^{-5}\) cm\(^{-2}\) s\(^{-1}\) sr\(^{-1}\) at the Galactic Center.

The diffuse emission is the only background for satellite experiments. Its large variation with Galactic coordinates
can make a weak source in Draco relatively brighter than strong emission from the Galactic Center, overwhelming
the numbers in Table III. For ACTs, however, the hadronic and electronic backgrounds are much larger and independent
of Galactic coordinates, so the hierarchy from Table III is retained. So, this raises the possibility that the Sagittarius
dSph might have a higher signal-to-noise ratio with ACTs, but the Draco dSph is more clearly seen from satellites.

V. THE DETECTORS

A. Minimum Detectable Flux

For the dSphs, the minimum detectable flux \(\Phi_\gamma\) is determined using the prescription that, for an exposure of \(t\)
seconds made with an instrument of effective area \(A_{\text{eff}}\) and angular acceptance \(\Delta\Omega\), the significance of the detection
must exceed 5\(\sigma\):

\[
\frac{\Phi_\gamma \sqrt{\Delta\Omega A_{\text{eff}}}}{\sqrt{\Phi_\gamma + \Phi_{\text{bg}}}} \geq 5.
\]

(16)

Here, \(\Phi_\gamma\) denotes the neutralino annihilation flux in cm\(^{-2}\) s\(^{-1}\) sr\(^{-1}\), while \(\Phi_{\text{bg}}\) is the background flux. Any detector sees
some photons from both dark matter annihilation and background, so the error in the measurement is \(\propto \sqrt{\Phi_\gamma + \Phi_{\text{bg}}}
and not \(\propto \sqrt{\Phi_\gamma}\). As pointed out in \[42\], the use of the latter formula overestimates the significance of any detection.

When studying the signal from discrete \(\gamma\)-lines, \(d\Phi_{\text{bg}}/d\Omega\) is the background flux falling under the annihilation line.
If the background has a differential spectrum \(d^2\Phi_{\text{bg}}/d\Omega dE = N_0 E^{-\delta}\), and if the energy resolution of the instrument
is \(\sigma_E/E\), then the background under a line at energy \(E_0\) (i.e., in the interval \([E_0 - \sigma_E, E_0 + \sigma_E]\) containing 68% of
the signal) is given by \[4\]:

\[
\frac{d\Phi_{\text{bg}}}{d\Omega} = \frac{N_0}{\delta - 1} E_0^{-\delta + 1} \times \eta(\sigma_E/E, \delta),
\]

(17)

with

\[
\eta(\sigma_E/E, \delta) = \frac{1}{(1 - \sigma_E/E)^{1-\delta}} - \frac{1}{(1 + \sigma_E/E)^{1-\delta}}.
\]

(18)

For ACTs, the background is the sum of three different power laws; for satellites, only the diffuse background is
needed.

In the literature, a number of different algorithms are used to define a detection of dark matter annihilation. Some
authors additionally require a minimum number of detected photons, though this number is set somewhat arbitrarily.
In \[4\], the minimum number is 25 for ACTs and 10 for satellite experiments; in \[43\], it is 100 for ACTs. In \[7\],
no minimum number of detected photons is required, which allows the possibility of a high significance detection
with a tiny number of received photons. In \[8\], a completely different strategy altogether is used: constraints on
supersymmetric parameter space are found by requiring that Draco’s flux be less than the least significant detection
(the Large Magellanic Cloud at 4\(\sigma\) \[44\]) above 1 GeV, resulting in a minimum flux for detection of \(10^{-8}\) cm\(^{-2}\) s\(^{-1}\). In this way,
the noise enters linearly into the expression. This explains why Tyler \[8\] excludes a large region in mSUGRA
parameter space from the non-detection of dSphs, despite the fact that the values of the integral \[44\] towards the
dSphs are quite low.
### B. Performance of the Detectors

The detector characteristics of the different experiments are summarised in Table VI. For definiteness, we use $\Delta \Omega = 10^{-5}\text{sr} \approx 0.1^\circ$ for the angular average when considering ACTs (appropriate for energies $\sim 100$ GeV) or GLAST (10 GeV), and $\Delta \Omega = 10^{-3}\text{sr} \approx 1^\circ$ for EGRET (10 GeV). Also important is the observation time, which is chosen as $t \approx 1$ yr for satellites. For the next generation ACTs, assuming four telescopes, we use an observation time $t \approx 100$ h and an exposure $A_{\text{eff}} = 4 \times 10^8$ cm$^2$. This seems reasonable, as CANGAROO [45] and the last phase of HESS [46] will have four telescopes, while VERITAS will have as many as seven [3]. MAGIC [47] uses a single 17 m mirror and has roughly the same performance as next-generation ACTs, but with a reduced threshold of 30 GeV.

### VI. RESULTS

The following plots show the parts of the supersymmetric parameter space that can be probed through the detection of a $\gamma$-ray signal from neutralino annihilations. We typically show the region to which GLAST and a generic second generation ACT will be sensitive. The plots found in [2] show the $\gamma$-ray flux in cm$^{-2}$s$^{-1}$ against photon energy. They are not appropriate for depicting the exclusion limits from observations of different parts of the sky because the flux changes and hence so do the points representing theoretical models. We prefer to use the type of plot presented in [7] with $N_\gamma(\sigma v)$ (which depends exclusively on the particle physics model) versus $m_\chi$ (although other quantities could be used as well).

From eq. (10), we write the condition for detection in a more convenient way for the plots:

$$N_\gamma(\sigma v) \geq \frac{4\pi m_\chi^2}{2\Delta \Omega A_{\text{eff}} t} \cdot \Phi_{\text{bg}}$$

Here, we see that increasing the angular acceptance $\Delta \Omega$ can increase the signal to noise ratio. In fact, if both signal and background are constant, the significance increases (and the minimum value of $N_\gamma(\sigma v)$ that can be probed decreases) as $\sqrt{\Delta \Omega}$. However, the signal is not constant as Table III shows, and the angular acceptance that maximizes the significance does not necessarily coincide with the minimum angular resolution of the detector. So the optimal strategy is to scan between the minimum angular resolution and the maximum field of view, choosing the field for which the signal to noise ratio is maximised. This depends on the position in the sky and on the type of profile. For instance, the distant Draco looks like a point source and the maximum signal is for the smallest angle possible. For Sagittarius, the optimal angle is $0.4^\circ$ for cored profiles and the smallest possible for cusped profiles. In order not to put too many lines in the plot, we have avoided drawing all the halo types and show only the extreme cases.

#### A. Discrete Lines

The annihilation of two neutralinos gives rise to two photons with energy $E_\gamma \approx m_\chi$. The region probed by the different experiments is shown in Fig. 1. Also shown are $\sim 1500$ points in the mSUGRA parameter space that comply with all the accelerator limits (including $b \to s\gamma, (g-2)_\mu$, and other accelerator limits [48] that are incorporated in DarkSusy). All the points, bar five, have spin-independent cross-section with protons or neutrons below $10^{-6}$ pb, thus compatible with limits set by the Edelweiss nuclear recoil detector, but not the disputed signal claimed by the DAMA experiment [49]. Also, the upward-going, neutrino-originated, muon showers have a flux of $\leq 10^4$ km$^{-2}$ yr$^{-1}$ (which according to Kurylov and Kamionkowski [50] is the limit set by super-Kamiokande).

As the figure shows, the discrete annihilation line is very unlikely to be observed, even with the next generation instruments. It is just about detectable for the most promising targets under the most optimistic assumptions – the Sagittarius or the Canis Major dSph galaxies assuming a Moore profile and using next generation ACTs. Other possible models (such as NFW or cored profiles) and targets (such as the Galactic Center) are much less propitious still. For GLAST, only one line is shown – namely that for the Canis Major dSph, but even this lies above all physical mSUGRA models and so provides no constraints. In particular, monochromatic lines from the Galactic Center are not visible to GLAST. The difference between this work and that of [2] is that the latter authors took a very high dark matter concentration in the center (the profile is just NFW, but the constant in front is set to ensure maximal flux given two weak constraints on the mass and the rotation curve). This causes the $\gamma$-ray flux in monochromatic lines from the Galactic Center as computed by [2] to be over two orders of magnitude greater than the values obtained in this paper.
FIG. 1: Exclusion limits for the discrete line $\chi\chi \rightarrow \gamma\gamma$. For all the experiments, only the most favorable cases are shown. The green, red and blue points correspond to mSUGRA models with $\Omega_{\text{CDM}}h^2$ in the range 0.005–0.2, as discussed in Section IIIA. The red points satisfy the more stringent WMAP constraints $0 < \Omega_{\text{CDM}}h^2 < 0.09$. The exclusion limits for $\chi\chi \rightarrow Z\gamma$ are very similar and not shown here.

B. Continuum Emission

The continuum emission comes from hadronization and subsequent pion decay. The programme DarkSusy \cite{33} uses results from the PYTHIA code \cite{51} to compute the photon multiplicity for each neutralino annihilation. Experimental sensitivities are shown in Fig. 2 for continuum emission above 1 GeV and 50 GeV.

The continuum emission above 1 GeV can yield some constraints. Although we have computed the curves for four targets (Draco, Sagittarius, Canis Major and the Galactic Centre) and for the full range of models in Section II, we give only the most promising results in the figures. The Draco, Sagittarius and Canis Major dSphs may yield interesting constraints – but only if their dark halo profiles are strongly cusped (the Moore and the NFW profiles both rule out some supersymmetric models). Unlike the case of the Milky Way, cusped profiles are still possible for the dSphs. Notice, however, that substituting cored power-law models for NFW or Moore profiles causes the exclusion limit to move well above the supersymmetric parameter space of interest. For $E_\gamma > 1$ GeV, only curves for GLAST are drawn, as ACTs are insensitive at such low energies.

Also shown in the upper panel of Fig. 2 is a line corresponding to the Milky Way observed at medium latitudes with the wide field of view of GLAST, as first suggested by Stoehr et al. \cite{6}. (This line lies almost exactly on top of the line for the Sagittarius dSph in the upper panel). Here, the Galaxy has been modelled with an isothermal power-law model, as opposed to the cusped models preferred by Stoehr et al. We agree therefore with the suggestion of Stoehr et al. that this is a promising target, as irrespective of whether the Galaxy is cusped or cored, there are always useful constraints on the supersymmetric parameters. Unfortunately, this attractive option is only available to GLAST and not for ACTs.

The lower panel of Fig. 2 shows the prospects for detection of continuum emission above 50 GeV. For ACTs, the Canis dSph is the best target, though a detectable signal will again only be measured if the density profile is strongly cusped. For GLAST, the Galaxy at medium latitudes again leads to some constraints, though not as strong as when continuum emission above 50 GeV is studied.
FIG. 2: Exclusion limits for continuum γ-ray emission above 1 GeV (top) and 50 GeV (bottom). Only the most favorable cases are shown. For $E_\gamma > 1$ GeV, only curves for GLAST are drawn, as ACTs are insensitive at such low energies. Above 50 GeV, curves are shown for both GLAST and second generation ACTs. The green, red and blue points correspond to mSUGRA models with $\Omega_{CDM}h^2$ in the range 0.005–0.2, as discussed in Section IIIA. The red points satisfy the more stringent WMAP constraints $0.09 < \Omega_{CDM}h^2 < 0.13$.

VII. CONCLUSIONS

If the dark matter present in the Universe is composed at least in part by the lightest supersymmetric particle, then this could manifest itself via γ-ray emission from pair annihilations. It is clearly important to estimate the likely magnitude of the neutralino annihilation signal. It is also important to identify the likely locations and spectral régimes in which the signal should be sought. This paper has provided new estimates of the signal towards the
Galactic Center and the nearby dwarf spheroidals using a variety of models.

There have been a number of recent calculations predicting that the neutralino annihilation flux from the inner Galaxy will be detectable with forthcoming satellites like GLAST and with second generation atmospheric Cerenkov telescopes (ACTs) [2]. These calculations assume that the cusped Navarro-Frenk-White (NFW) models for the Milky Way halo hold good. This assumption is in contradiction with a substantial body of astrophysical evidence about the inner Galaxy [13, 14, 15]. In any case, even if the Milky Way halo was originally of NFW form, the formation of the disk and bulge will have reprocessed the primordial dark matter distribution [16]. In contradiction with earlier results, we do not find the prospects of detecting the annihilation flux from the Galactic Center to be particularly promising. In particular, the γ-ray line coming from the the γγ and Zγ final states is not detectable either with second generation ACTs or with the GLAST satellite. We caution that many of the recent estimates of high flux are sensitiively dependent on the assumptions made regarding the innermost structure of the dark halo. Even the best numerical simulations have difficulty in resolving structures on scales less than 1 kpc, and so the inner profile is always found by extrapolation.

The high mass-to-light ratios of the Local Group dwarf spheroidals (dSphs) makes them attractive targets. Cusped profiles like NFW are not presently ruled out for dSphs like Sagittarius or Draco. It may be that the visible dwarf galaxy lies entirely within the central parts of a cusped dark matter halo. If so, then the optimum targets are the Sagittarius and Canis Major dSphs. The detection of monochromatic lines is still extremely difficult, but the GLAST satellite may detect excess continuum γ ray emission. This is of course a less distinctive feature than a sharp line. In particular, if the Sagittarius or Canis Major dSphs have a strongly cusped dark halo profile (ρ ∼ r−1.5 or ρ ∼ r−1), then some regions of supersymmetric parameter space can be ruled out. Again, however, this conclusion only holds good if the dark halo profile is cusped. Using a cored isothermal-like model for the dark halo, even the Sagittarius and Canis Major dSphs may be invisible to GLAST and second generation ACTs.

Unlike Bergstrom et al. [2], we do not find the Galactic Center to be a promising location. Partly, this is because we believe that the Milky Way does not have a strongly cusped profile based on the available astrophysical evidence [14, 15, 17]. Partly, this is because Bergstrom et al. chose a generous overall normalisation anyhow — they used the NFW model corresponding to the maximum flux which satisfies two weak constraints on the mass and the rotation curve. Accordingly, the local dark matter density is as high as ∼ 0.6 GeV cm−3 in their model. When the circular velocity curve of such a halo is combined with that for the disk and bar, then it necessarily violates the constraint on the Galactic rotation curve in the inner parts. One important caveat of our results — however — is that the possible effects of a central black hole are not included in our calculations. Here, we merely note that the observability of any expected signal depends on the manner in which the black hole grows [53, 54].

Stoehr et al. [6] have also recently emphasised that the γ-ray emission from the Galactic Center may have been overestimated by the use of too strongly cusped profiles. They suggest that the galaxy at moderate latitudes (|b| > 10◦) may also be a good target for detecting the continuum emission (they do not study the line emission). This is not really an option for ACTs with their small field of view. However, it is an attractive possibility for GLAST, as the continuum emission is detectable irrespective of uncertainties in halo structure. For ACTs, the best targets remain the Sagittarius and Canis Major dSphs.

Very recently, the Large Magellanic Cloud (LMC) has been suggested as another likely target [29]. Judging from [52], the average mass to light ratio of the LMC within 8.9 kpc is only ∼ 3 (as opposed to ∼ 100 for the compact dSphs). This is an upper limit to the central mass to light ratio. In other words, much as in the Milky Way, dark matter dominates the outer parts of the LMC and is responsible for the asymptotic flatness of the ratio curve. However, the central parts of the LMC are dominated by the luminous bar and disk. The assumption that the dark halo dominates the gravitational potential everywhere is therefore not valid. Hence, the procedure used in [20] of fitting the rotation curve to a NFW dark halo is flawed. The gravitational potential of the gas and stellar disk and bar simply cannot be ignored in the central regions.

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| Energy     | HESS (I) | VERITAS | MAGIC | EGRET | GLAST       |
|------------|----------|----------|-------|-------|-------------|
| Energy     | 40 GeV-10 TeV | 50 GeV-10 TeV | 30 GeV-10 TeV | 20 MeV-30 GeV | 20 MeV-300 GeV |
| $\sigma_{E/E}$ | $\approx 10\%$ | $\approx 15\%$ | $\approx 20\%$ | $< 10\%$ | $\approx 5\% \text{ > 10 GeV}$ |
| $A_{\text{eff}}$ (cm$^2$) | $4 \times 10^6$ (>100 GeV) | $4 \times 10^6$ (>100 GeV) | $4 \times 10^6$ (>100 GeV) | $1.5 \times 10^4$ | $10^4$ |
| $\Phi_{\text{min}}$ (cm$^{-2}$s$^{-1}$) | $8 \times 10^{-12}$ (>100 GeV) | $9 \times 10^{-12}$ (>100 GeV) | $\approx 10^{-11}$ (>100 GeV) | $10^{-7}$ (>100 MeV) | $3 \times 10^{-9}$ (>100 MeV) |
| Ang. res. (single $\gamma$) | $< 0.1^\circ$ at 100 GeV | $< 0.1^\circ$ at 100 GeV | $\approx 0.2^\circ$ | $< 5.8^\circ$ at 100 MeV | $2^\circ$ at 100 MeV |
| Field of view | $4.3^\circ - 5^\circ$ | $3.5^\circ$ | $\approx 5^\circ$ | 0.5 sr | 2.4 sr |

TABLE V: Performance of the gamma-ray detectors. Numbers quoted correspond to $5\sigma$ sensitivity after 100 hours of observation for ACTs and 1 yr for GLAST.