Spin Waves and Magnetic Exchange Hamiltonian in CrSBr

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CrSBr is an air-stable two-dimensional (2D) van der Waals semiconducting magnet with great technological promise, but its atomic-scale magnetic interactions—crucial information for high-frequency switching—are poorly understood. An experimental study is presented to determine the CrSBr magnetic exchange Hamiltonian and bulk magnon spectrum. The A-type antiferromagnetic order using single crystal neutron diffraction is confirmed here. The magnon dispersions are also measured using inelastic neutron scattering and fit rigorously the excitation modes to a spin wave model. The magnon spectrum is well described by an intra-plane ferromagnetic Heisenberg exchange model with seven nearest in-plane exchanges. This fitted exchange Hamiltonian enables theoretical predictions of CrSBr behavior: as one example, the fitted Hamiltonian is used to predict the presence of chiral magnon edge modes with a spin-orbit enhanced CrSBr heterostructure.

1. Introduction

Two-dimensional (2D) magnetism has long been a topic of theoretical investigation, but only recently has it become experimentally accessible through van der Waals materials.[1,2] With monolayer magnetism preserved through magnetic anisotropy, these materials promise to yield cleaner experimental realizations of theoretical states, novel spintronic devices, and new topological phases of matter.[3,4] However, accurately predicting the magnetic properties and excitations requires a detailed knowledge of the magnetic exchange Hamiltonian.

A promising 2D van der Waals magnet is CrSBr. CrSBr forms 2D layers of magnetic Cr$^3+$ ions forming a rectangular lattice, as shown in Figure 1. In bulk, it orders magnetically at $T_N = 132$ K$^{[5–7]}$ with A-type antiferromagnetism: ferromagnetic planes polarized along the $b$-axis, alternating in orientation for an overall antiferromagnetic (AFM) order, and becoming ferromagnetic (FM) in the monolayer limit.[8] This material is air-stable and has a semiconducting gap low enough to gate with realistic electric fields.[6,9] There is also intricate interplay between electronic transport, optical properties, and magnetism,[10,11] with the potential for exploiting both spin and charge degrees of freedom for technological purposes.[12] To understand, predict, and ultimately exploit the spin transport properties of CrSBr, it is necessary to know the magnetic exchange Hamiltonian between Cr ions and the resulting magnon dispersions. In particular, the high-frequency behavior of the magnon bands is critical to understanding the short-time behavior relevant for electronic switching and information processing. In this study, we measure the static magnetic structure and the high energy magnon dispersions, experimentally determine the spin exchange Hamiltonian using inelastic neutron scattering, and then use this Hamiltonian to predict the presence of chiral edge modes in layered heterostructures. In this way, using bulk probes yields crucial information to predict monolayer behavior.

2. Results and Analysis

2.1. Static Magnetism

The single crystal neutron diffraction is shown in Figure 2 and confirms the ground state magnetic order in ref. [7]: below a transition temperature of 132.3(6) K, new Bragg peaks appear at half-integer $\ell$ positions in accord with (00$\ell$) magnetic order. In the Supporting Information, we refine the Bragg intensities and show they indicate A-type antiferromagnetism in Figure 1. At temperatures near $T_N$, a streak of scattering appears at ($0, 1, \ell$), signaling 2D magnetic correlations in the $ab$-plane. Tracking the 2D correlations as a function of temperature, we see they peak at $T_N$, but with significant 2D magnetic correlations above $T_N$.

The 3D Bragg intensity versus temperature follows a smooth curve between $T_N$ and 5 K. Although CrSBr samples show a sample-dependent discontinuity in magnetic susceptibility at 30 K,[10] no such feature is observed in the neutron diffraction. Furthermore, aside from a larger static moment at 5 K, we also find no difference between 80 and 5 K refined magnetic structures. Thus we conclude, as did ref. [7], that the 30 K discontinuity is not associated with a change in the spatially-averaged
magnetic order. This is consistent with the proposal in ref. [10] that the susceptibility discontinuity is due to local or impurity spins. Fitting the 3D Bragg intensity to an order parameter curve, we find a critical exponent \( \beta = 0.231 \pm 0.006 \). This is far from the theoretical 3D Heisenberg critical exponent \( \beta = 0.36 \). Instead, this is remarkably close to the critical exponent \( \beta = 0.231 \) derived for the 2D XY model via Kosterlitz–Thouless (K–T) theory, showing very 2D exchange interactions with easy-plane anisotropy, in accord with expected Van der Waals behavior.

### 2.2. Dynamic Magnetism

Several plots of CrSBr inelastic neutron scattering data are shown in Figure 3. Because of the small sample mass, there is substantial background noise from phonon scattering in the aluminum sample holder. Nevertheless, the magnon modes are clearly distinguished by i) their symmetries following the CrSBr reciprocal lattice units, ii) their intensities following a magnetic form factor with intensity largest near \(|Q| = 0\), and iii) comparison with a measured background (see Experimental Section).

The magnon dispersions in the \((hk0)\) plane reach a maximum energy of \( \approx 0.45 \) meV. Within an energy resolution of \( \pm 0.5 \) meV FWHM in the \( E_\text{f} = 20 \) meV data (Figure 3d), the modes are gapless at \( h + k = \) even integer points in reciprocal lattice units (RLU). This lack of observable gap evidences highly isotropic magnetism, as one expects for \( S = 3/2 \) Cr\(^{3+}\). This comports with density functional theory predictions\[13\] and recent photon measurements finding \( Q = 0 \) magnon gaps of 0.102(3) and 0.141(4) meV\[16\] as well as magnetization measurements finding a maximum anisotropy of 0.144 \( \mu \)eV at 2 K (c-axis compared to b) in CrSBr (see Supporting Information\[17\]): too small to be resolved in this experiment.

In the \( \epsilon \)-direction, we find no measurable dispersion out of plane at all \( h \) and \( k \), as shown in Figure 4. This evidences very weak inter-plane magnetic exchange, as one would expect for a highly 2D system (see the Supporting Information for further details\[17\]). This is consistent with the photon excitation study in ref. [16] which finds an interlayer exchange \( < 0.01 \) meV, as well as density functional calculations in ref. [18] which finds a CrSBr interlayer magnetic interaction three orders of magnitude weaker than the in-plane interactions. Because the modes are flat with \( \epsilon \), all in-plane scattering data presented here is integrated over \(-1 < \epsilon < 1\) RLU to maximize the magnon mode visibility.

### 2.3. Fitting the Exchange Hamiltonian

We determined the CrSBr magnetic exchange constants from this scattering data by performing a fit to a linear spin wave theory (LSWT) model. The spin wave model for a bipartite ferromagnetic lattice is calculated following ref. [19] using the Hamiltonian

\[
H = \sum_{ij} J_{ij} \vec{S}_i \cdot \vec{S}_j
\]

where \( \vec{S}_i \) are vectors of length \( |\vec{S}| = 3/2 \) and \( J_{ij} \) are magnetic exchange constants between pairs of spins. Because many exchanges are symmetry-equivalent, we write \( J_n \) where \( n \) is the neighbor number. The fitted neighbors \( n \) are shown in Figure 1b.

To constrain the fit, we extracted 188 unique \( Q \) and \( hwo \) points by fitting constant \( |Q| \) cuts of the magnon modes to Gaussian profiles in energy across 11 different data slices, using only regions where the magnons are clearly distinguishable from background (see Supporting Information for details\[17\]). We then defined a global reduced \( \chi^2 \) function based on magnon mode energies at those \( Q \) points, minimizing \( \chi^2_{\text{red}} \) by varying \( J_n \) using Scipy’s optimization package\[20\].

To systematically determine the number of exchange constants to include in our model, we fitted the magnon modes to a spin

Figure 1. CrSBr crystal structure. a) The crystal structure and Cr\(^{3+}\) magnetic order, ferromagnetic in-plane but layered in alternating directions for a bulk antiferromagnetism is shown. b) The Cr neighbors in the plane from the central red atom, numbered in order of bond length (neighbors 6, 9, 10, and 12 are between planes) are shown.

Figure 2. Single crystal CrSBr neutron diffraction. a– d) The temperature evolution of the \((0,1,3/2)\) Bragg peak (which is smeared out in \( Q_z \), due to crystal twinning) is shown. Above and near the phase transition, a streak of scattering along \( \epsilon \) appears, signaling two-dimensional (2D) magnetic correlations. We track the 3D and 2D correlations using the red and white boxes in panels (a–d) (the black box is the background), plotted in panel (e). The 2D correlations peak at the ordering temperature \( T_N = 132.2(6) \) K, and decrease at lower temperatures. The fitted order parameter curve is shown in gray, with a fitted \( \beta = 0.231(6) \). Error bars indicate one standard deviation uncertainty.

Figure 3. (a) CrSBr inelastic neutron scattering data. The 2D correlations peak at the ordering temperature \( T_N = 132.2(6) \) K, and decrease at lower temperatures. The fitted order parameter curve is shown in gray, with a fitted \( \beta = 0.231(6) \). Error bars indicate one standard deviation uncertainty.

Figure 4. Single crystal CrSBr neutron diffraction. a– d) The temperature evolution of the \((0,1,3/2)\) Bragg peak (which is smeared out in \( Q_z \), due to crystal twinning) is shown. Above and near the phase transition, a streak of scattering along \( \epsilon \) appears, signaling two-dimensional (2D) magnetic correlations. We track the 3D and 2D correlations using the red and white boxes in panels (a–d) (the black box is the background), plotted in panel (e). The 2D correlations peak at the ordering temperature \( T_N = 132.2(6) \) K, and decrease at lower temperatures. The fitted order parameter curve is shown in gray, with a fitted \( \beta = 0.231(6) \). Error bars indicate one standard deviation uncertainty.
wave model beginning with only two neighbors, and increasing the number of neighbors up to the 17th neighbor exchange (excluding all inter-plane exchanges), re-fitting for each new neighbor. We find that additional neighbors improve the best fit $\chi^2_{\text{red}}$ value up to the eighth neighbor (excluding $J_6$, which is between CrSBr planes). Including neighbors beyond eight does not improve $\chi^2_{\text{red}}$ by a significant amount, as shown in Figure 5. Furthermore, we find that the statistical uncertainty of all exchanges beyond the eighth neighbor overlap with zero, and so we truncate our model at the eighth neighbor exchange and consider all further exchanges to be negligible in CrSBr.

The best fit CrSBr Hamiltonian is given in Table 1. Uncertainty was calculated via a $\Delta \chi^2_{\text{red}} = 1$ contour for a one standard deviation statistical uncertainty, see Supporting Information for details. This was added in quadrature to the systematic uncertainty.

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**Table 1.** Best fit Hamiltonian exchange parameters for CrSBr. Uncertainty indicates one standard deviation.

| Exchange | Best Fit Value ± Uncertainty |
|----------|-----------------------------|
| $J_1$    | $-1.90 ± 0.10$ meV          |
| $J_2$    | $-3.38 ± 0.06$ meV          |
| $J_3$    | $-1.67 ± 0.10$ meV          |
| $J_4$    | $-0.09 ± 0.05$ meV          |
Figure 6. Effect of nearest neighbor DM interaction on the CrSBr dispersion. Panel (a) shows the CrSBr data along (0.75, k, 0), and panels (b) and (c) show the LSWT predictions with and without a DM term. The DM induces a gap at k = 1.5, but no gap is resolvable in the data. This constrains the nearest neighbor DM term to be <0.8 meV.

uncertainty from truncating the model to the eighth neighbor exchange, taken to be the range of parameter variation between n = 11 and n = 17 fits. We simulated the neutron cross section for this best fit Hamiltonian using SpinW software package,[22] plotted in Figure 3e–h. The agreement between theory and experiment is remarkable good for this isotropic exchange model. However, asymmet-
ric Dzyaloshinskii–Moriya (DM) exchange is expected to be very weak in Cr3+ because of its small spin-orbit coupling, such mode splitting was observed in CrI3 with a fitted DM interaction of 0.31 meV.[4] Thus it may be that a weak DM exchange also plays a role in CrSBr.

To test whether the DM exchange is significant, we added a nearest neighbor DM exchange to our fitted model and allowed it to vary along with the other fitted parameters. No mode splitting is observed in our data, so any split modes are below the experimental resolution (see Figure 6). We find that the best fit nearest neighbor DM term is unstable against the number of neighbors n included in the model, varying between 0.0 and 0.4(4) meV. We also find that the uncertainty overlap with zero for all n. Furthermore, the best fit χ2_red slightly worsens when the DM exchange is added: χ2_red = 13.5819 with D1, χ2_red = 13.5818 without D1 (see Supporting Information[17]). DM exchange is symmetry-forbidden on the second neighbor bond, but is allowed on the third neighbor bond where the signature is also mode splitting at the Brillouin zone boundary. No such splitting is resolvable in the data. Therefore, we consider the DM exchange to be negligible for CrSBr. While it is presumably nonzero, it is too small to resolve using this data.

3. Discussion

These results show that the CrSBr spin exchange Hamiltonian can be accurately approximated as a single-layer ferromagnet. Single-ion anisotropy, inter-plane exchange, and anisotropic exchange are all too small to resolve, leaving the exchange constants in Table 1 as an effective minimal model for the high frequency (short time) behavior of CrSBr. The fitted exchange parameters are almost uniformly ferromagnetic, with very similar exchange in the a- and b-directions, evidencing very 2D magnetism (in contrast to the quasi-1D electronic bands[24]). The CrSBr magnetic Hamiltonian having significant magnetic exchange out to the eighth neighbor is somewhat surprising, but is consistent with the strong Cr–S and Cr–Br covalency[18] which gives opportunity for extended orbital overlap.

We can compare this with first principles predictions for CrSBr. Guo et al.,[25] used density functional theory to predict J1 = −1.72 meV, J2 = −3.25 meV for CrSBr (normalized to the S = 3/2 vector convention we use in Equation (1)). This is very close to the fitted J1 = −1.9(1) meV and J2 = −3.38(6) meV, showing good agreement between experiment and theory. Similarly, Wang et al.[15] and Yang et al.[18] also used density functional theory on to predict weak CrSBr single-ion anisotropy (too weak to be measured with our measurements), although both their calculated CrSBr bulk exchange constants are larger than we observe in experiment.

Because the CrSBr semiconducting gap is 1.25(7) eV[6] (14500 K), the effects of thermally populated conduction-mediated exchange will be very minor between 5 and 300 K. Some exchange constant shifts with lattice expansion is possible, but such effects will also be minor.[26] Therefore we expect the magnetic exchange constants in Table 1 can be considered approximately correct at all temperatures below 300 K.

3.1. Calculating Edge Modes

Having determined the spin exchange Hamiltonian for CrSBr, we can begin using it to calculate relevant quantities. Among many spintronics proposals are “topological magnonics”: using magnon edge modes for low-dissipation transport and switches.[27] Magnon edge states, which only exist on the edge of a 2D material, generally have different dispersions than those in the bulk. For certain lattice geometries and Hamiltonians, the edge magnons can be “chiral”, with a directional velocity preference based on the terminating surface.[28] Such chiral edge modes can be induced in ferromagnets via an anisotropic DM interaction.[29]

In 2D materials, it is possible to increase the anisotropy via proximity effects with layers of heavy atoms, thereby enhancing spin-orbit interaction.[30,31] This has been powerfully demonstrated with graphene heterostructures.[12,33] Because spin orbit interaction drives the asymmetric DM exchange,[21] it is possible to increase the CrSBr DM interaction via layering with a strong spin-orbit coupled material.[34,35]

To examine the effect of large DM exchange on the surface magnon modes of CrSBr, we performed large box spin wave simulations using SpinW.[22] We generated a lattice 12 unit-cells in extent along the a-b-axis with periodic boundary conditions along a and c. We then performed LSWT calculations with and without periodic boundary conditions along b using the Hamiltonian in Table 1, with and without D1 (DM on the first neighbor) exchange. The results are plotted in Figure 7. The surface modes are clearly visible as the modes at lower energies than the bulk dispersions, and which disappear when periodic boundary conditions are applied.

Without DM interaction, the surface modes have a sinusoidal character, with the same dispersion for both surfaces. However,
We then use this calculated spin wave model to predict the presence of a chiral edge mode if the nearest neighbor DM exchange interaction could be enhanced by proximity effects. These results suggest potential topological edge modes in CrSBr heterostructures is a future direction worth exploring.

5. Experimental Section

Sample Synthesis: The following reagents were used as received unless otherwise stated: chromium powder (99.94%, ~200 mesh, Alfa Aesar), sulfur pieces (99.995%, Alfa Aesar), bromine (99.99%, Aldrich), and chromium dichloride, (anhydrous, 99.9%, Strem Chemicals).

For a starting material, high quality CrBr₃ was synthesized from the elements (Cr: 1.78 g, 34.2 mmol and Br₂: 8.41 g, 52.6 mmol) with one end of the tube maintained at 1000 °C and the other side at 50 °C with a water bath. Details of the reaction can be found in ref. [16]. Caution: One end of the tube must be maintained below 120 °C to prevent the tube from exploding from bromine overpressure.

A modified procedure from ref. [16] was used to synthesize large single crystals of CrSBr. Chromium (0.174 g, 3.35 mmol), sulfur (0.196 g, 6.11 mmol), and CrBr₃ (0.803 g, 2.75 mmol) were loaded into a 12.7 mm O.D., 10.5 mm i.D. fused silica tube. The tube was evacuated to a pressure of ~30 mtorr and flame sealed to a length of 20 cm. The tube was placed into a computer-controlled, two-zone, tube furnace. The source side was heated to 850 °C in 24 h, allowed to soak for 24 h, heated to 950 °C in 12 h, allowed to soak for 48 h, and then cooled to ambient temperature in 6 h. The sink side was heated to 950 °C in 24 h, allowed to soak for 24 h, heated to 850 °C in 12 h, allowed to soak for 48 h, and then cooled to ambient temperature in 6 h. The crystals were cleaned by soaking in 1 mg mL⁻¹ of CrCl₃ aqueous solution for 1 h at ambient temperature. After soaking, the solution was decanted and the crystals were thoroughly rinsed with DI water and acetone. Residual sulfur residue was removed by washing with warm toluene.

Neutron Experiments: The neutron diffraction of CrSBr was measured with the TOPAZ diffractometer[16] at Oak Ridge National Laboratory’s SNS. TOPAZ used the neutron wavelength-resolved Laue technique for data collection to measure a 3D volume from a stationary single-crystal sample. Diffraction study was made on a plate-shaped single crystal with dimensions 5 × 2.5 × 0.8 mm, oriented with the c-axis vertical. Sample temperature was controlled by a Cryomech P415 pulse tube cryocooler. Data were collected using crystal orientations optimized with the CrystalPlan software in the range 36° to 180°[41] at 200, 80, and 5 K. An order parameter curve heating from 5 to 200 K at a fixed rotation angle of 3.56° was also measured. As explained in detail in the Supporting Information, the Basirep[38] and JANA software packages[39] were used to perform a refinement to the magnetic Bragg intensities and a static ordered moment of 3.56(2) μB at T = 5 K was found. This is consistent with the theoretical static moment of a S = 3/2 Cr²⁺ ion: g(3/2) = 3 μB plus a small orbital contribution.

The inelastic neutron spectrum of CrSBr was measured using the SEQUOIA spectrometer[40-41] at Oak Ridge National Laboratory’s SNS.[42] The sample consisted of 13 coaligned crystals with a total mass of 300 mg, aligned with the c-axis vertical and glued to an aluminum plate using CYTOP glue[43] (a picture is shown in the Supporting Information). The sample was mounted in a closed cycle refrigerator and cooled to a base temperature of 5 K. The scattering with incident energies E_i = 70 meV and E_i = 70 meV was measured.

For the SEQUOIA neutron measurements, the 70 chopper was set at 60 Hz, and high flux Fermi 1 chopper at 240 Hz was used, for E_i = 70 meV, and the neutron absorbing slits in front of the sample were set to provide the beam size 44 mm wide and 6 mm tall. The spectra was also measured with E_i = 20 meV neutrons using high resolution Fermi 2 chopper at 240 Hz, 70 chopper at 60 Hz. For the E_i = 70 meV data the sample was rotated a full 180° in 1° steps, but for the E_i = 20 meV data only 35° was rotated to capture the bottom of the dispersion around (1,1,0).

4. Conclusion

In conclusion, we have measured the magnetic diffraction of CrSBr and confirmed the 2D XY A-type antiferromagnetism. We also measured inelastic spin wave spectra of CrSBr and fitted the observed magnon modes to a linear spin wave model. We find a minimal magnetic exchange model with seven in-plane exchanges accurately reproduces the experimental spectra, with both single-ion and exchange anisotropy being too small to resolve. We also find no visible dispersion in the out of plane direction, confirming the highly 2D nature of CrSBr. We anticipate this experimentally derived Hamiltonian to be useful for calculating the behavior of this material in heterostructures and spintronic devices.
Supporting Information
Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest
The authors declare no conflict of interest.

Data Availability Statement
Spin wave data is available for download at doi.org/10.13139/ORNLNCCS/1869252.

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