Proficiency testing for calibration of multimeter

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Abstract. In 2018 and 2019, CT2M organize an inter-laboratory comparison of multimeter calibration in which 27 Europeans laboratories participated. Among them were calibration laboratories (accredited or not) but also laboratories performing themselves the calibrations of their multimeter. The principle of this inter-laboratory comparison is to circulate a multimeter from one laboratory to another in order to compare the calibration results (including correction and calibration uncertainty). The processing of the results is carried out according to the ISO 13528 statistical principles and in compliance with the requirements of ISO 17043. A final report in 2019 will indicate to the participants all the results in anonymous way and the performance scores to evaluate the ability of laboratories to carry out this calibration. This article will present the organization of this inter-laboratory comparison as well as the results obtained.

1 Introduction

Accreditation body require accredited laboratories to regularly participate in inter-laboratory comparisons (ILC) to prove their ability to perform tests or calibrations. Since 2014, CT2M organized inter-laboratory comparison in various fields to meet that need.

In 2018, an inter-laboratory comparison was organized for the calibration of multimeter. 27 laboratories took part in this round which took place from April 2018 to April 2019. The participants were calibration laboratories (accredited or not) as well as testing laboratories carrying out internal calibrations and / or controls of their multimeter.

This proficiency testing scheme was organized in accordance with the requirements of ISO 17043 and the results processing and participant performance study were conducted according to the principles of ISO 13258. The results obtained are presented in this paper.

2 Organisation of the proficiency texting round

2.1 Proficiency testing items

The comparison is based on the calibration of a multimeter (HP 34401A) chosen to cover the most commonly used range and calibration points.
To ensure the stability of the multimeter during the ILC round, an accredited reference laboratory, which was not part of the participants, calibrated at the beginning and at the end of the round.

2.2 Procedure of the proficiency testing

Calibration method is not imposed. Laboratories were allowed to choose their internal method. Each laboratory used its procedure and was free to choose the number of répétitions. Calibration points are detailed as follows (Table 1).

Direct current:

| Tests    | Calibration points          |
|----------|-----------------------------|
| Voltage  | 10mV, 100mV, 1V, 10V, 100V, 1000V |
| Current  | 10µA, 100µA, 1mA, 10mA, 100mA, 1A |
| Resistance | 10 Ω, 1kΩ, 10kΩ, 100 kΩ, 1MΩ, 10MΩ |

Alternatif current:

| Tests    | Frequency | Calibration points |
|----------|-----------|--------------------|
| Voltage  | 100 Hz    | 10mV, 100mV, 1V, 10V, 100V, 1000V |
| Current  | 100 Hz    | 1mA, 10mA, 100mA, 1A |

Table 1. Calibration points for ILC.

Informations about range, configuration and frequency were given to participants.

The participants had to determine the correction of each calibrated point. In addition, the following information could be mentioned:

✓ The expanded calibration uncertainty (k=2),
✓ Influence factors considering for the uncertainty calculation,
✓ Environmental conditions during calibration.
3 Method for data analysis

3.1 Hypothesis for data analysis

The purpose of the proficiency testing is to conduct an assessment of laboratory performance by comparing their results with each other and against a reference value. Assumptions were considered for the data analysis to make consistent conclusions on the results.

In accordance with the reference standards [1] [2] [3], the assumption of a normal distribution of the data series has been made. This hypothesis has been verified for all results using the following two methods:

 ✓ Graphical Method (normal probability plot)
 ✓ Statistical method (Shapiro-Wilk)

The Grubbs test was performed on all corrections determined by each of the participant. The purpose of this test is to identify a laboratory with an incoherent result compared to other participants. The test involves calculating the Grubbs parameter (G) and comparing it to the critical Grubbs values of ISO 5725-2 [3].

Application of this GRUBBS test highlighted:
- 11 outliers in continuous tension especially on low values
- 7 outliers in alternative tension
- 7 outliers in continuous current
- 11 outliers in alternating current especially on strong values
- 14 outliers in resistance.

3.2 Assigned values and standard deviations

3.2.1 Reference value and uncertainty

The reference values of this proficiency testing were obtained by a reference laboratory that is accredited according to ISO/IEC 17025.

It calibrated the multimeter at the beginning and at the end of the ILC round. The reference value \( x_{\text{ref}} \) is the average of both corrections.

Its associated uncertainty \( U_{\text{ref}} \) takes into account the uncertainty of the reference laboratory as well as the possible drift of the multimeter between the beginning and the end of the round.

3.2.2 Robust mean and robust standard deviation

The robust mean \( x^* \) and the robust standard deviation \( S^* \) are determined using the algorithm A defined in ISO 13528. The robust average and standard deviation are used to evaluate the Z-score of each participant.
The Table 2 shows the parameters obtained for all the tests:
- $x^*$: robust average
- $S^*$: robust standard deviation
- $U_{x^*}$: uncertainty on the robust average

### 3.2.3 Comparison between the robust averages and the reference values

When organizing an inter-laboratory comparison, it is important to ensure that the robust averages of the participants results are not significantly different from the reference values.

For instance, the table (tab.2) below show a good correspondence between the robust means and the reference values for calibration points.

In table, symbols below correspond to the following data:
- $x^*$: robust average
- $s^*$: robust standard deviation
- $U_{x^*}$: uncertainty on the robust average ($k=2$)
- $x_{ref}$: reference value
- $U_{ref}$: uncertainty on the reference value ($k=2$)
- $E_n$: Number $E_n$

| Range | Calibration points | $x^*$  | $s^*$  | $U_{x^*}$ | $x_{ref}$ | $U_{ref}$ | $E_n$ |
|-------|---------------------|--------|--------|-----------|-----------|-----------|-------|
| 100 mV| 10 mV               | 1,88E-07 | 4,90E-07 | 2,36E-07 | 1,50E-07 | 1,42E-07 | 0,14  |
|       | 100 mV              | 9,58E-07 | 1,99E-06 | 9,56E-07 | 1,70E-06 | 7,02E-07 | 0,63  |
| 1 V   | 0,1 V               | 5,84E-07 | 1,07E-06 | 5,25E-07 | 1,00E-06 | 1,30E-06 | 0,30  |
|       | 1 V                 | 7,15E-07 | 3,19E-06 | 1,54E-06 | 0,00E+00 | 4,00E-06 | 0,17  |
| 10 V  | 1 V                 | 6,16E-08 | 3,57E-07 | 1,75E-07 | 0,00E+00 | 1,30E-05 | 0,00  |
|       | 10 V                | -1,85E-06 | 2,22E-05 | 1,07E-05 | -5,00E-06 | 4,36E-05 | 0,07  |
| 100 V | 10 V                | 1,67E-05 | 5,79E-05 | 2,84E-05 | -5,00E-05 | 1,42E-04 | 0,46  |
|       | 100 V               | -6,63E-06 | 3,03E-04 | 1,46E-04 | -1,00E-04 | 5,29E-04 | 0,17  |
| 1000 V| 100 V               | 1,35E-04 | 5,95E-04 | 2,92E-04 | 5,00E-04 | 1,42E-03 | 0,25  |
|       | 1000 V              | -2,16E-03 | 7,90E-03 | 3,95E-03 | -9,50E-03 | 4,36E-03 | 1,25  |

Results in V

**Table 2. assigned values in DC voltage**

The number $E_n$ highlights the difference between the robust average with its uncertainty and the reference value with its uncertainty (Table 2). The number $E_n$ between both the results are correct for all the calibration points.

It is therefore possible to conclude that there is no significant difference between the reference values (obtained by the reference laboratory) and the robust averages (participants results).
4 Participant results

For instance, the results for calibration point 1000V range 1000V are presented in the following graphs (fig.1). They show the correction and their uncertainties associated with k=2 (error bars).

![Fig. 1. Correction 1000V Range 1000V](image)

For each calibration point, a histogram also shows the frequency of the results (number of laboratories) according to the class of values.

5 Participant performance

The laboratories performance is determined by the Z-score that is a standardized measure of the bias. This performance score is calculated using the following formula:

\[ Z = \frac{x_{lab} - x^*}{S^*} \]  (1)

The reference value \( x^* \) is the robust average of the participants results, the value \( x_{lab} \) is the value obtained by the laboratory and the parameter \( S^* \) is the robust standard deviation of the participants results.

For each participant, the z-scores were calculated for each calibrated points (Fig. 2 – range 1000V). The Z-scores between -2 and -3 or 2 and 3 correspond to isolated result. The Z-scores less than -3 or greater than 3 correspond to discordant result.

![Fig. 2. Z-scores of each participant (Range 1000V)](image)
If a laboratory obtains a positive (or negative) Z-score, this highlights an overall bias (systematic error) on the calibration process compared to the average of the participants.

An interpretation of the results in relation to the reference value was also performed using the number $En$. It is a parameter that lead to evaluate the difference between 2 values. The values are compared taking into account their associated expanded uncertainties. The results of the participants are therefore compared to the reference value. The number $En$ is calculated using the following formula:

$$En = \frac{x_{lab} - x_{ref}}{\sqrt{U_{lab}^2 + U_{ref}^2}}$$  \hspace{1cm} (2)

- $x_{ref}$ is the reference value (reference laboratory),
- $x_{lab}$ is the laboratory value,
- $U_{ref}$ is the uncertainty ($k=2$) on the reference value,
- $U_{lab}$ is the uncertainty ($k=2$) on the laboratory value.

The Figure 3 shows the results of all the numbers $En$ for the calibrated point range 1000V. If a laboratory obtains a positive (or negative) number $En$ on all the calibration points, this highlights an overall bias (systematic error) on the calibration process compared to the reference value. This bias is all the more so important as the number $En$ is far from 0.

The interpretation of the number $En$ must be done with caution. Indeed some laboratories have significant uncertainties, which leads to a correct standardized deviation (less than 1 or more than -1) despite significant bias compared to the reference value.
6 Conclusions

This inter-laboratory comparison bringing together a sufficient number of laboratories made it possible to highlight conclusions.

The results of the participants were exploited and performance criteria were provided to participants so that they could either validate their calibration method as accreditation bodies, or improve it by triggering actions to correct a possible bias.

References

1. ISO 13528 October 2015: Statistical methods for use in proficiency testing by interlaboratory comparisons
2. EN ISO/CEI 17043 April 2010: Conformity assessment - General requirements for proficiency testing
3. ISO 5725-2 December 1994 : Accuracy (trueness and precision) of measurement methods and results - Part 2: Basic method for the determination of repeatability and reproducibility of a standard measurement method