Search for RS gravitons via $W_L W_L$ decays

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(Dated: July 5, 2008)

Abstract

The original Randall-Sundrum (RS) model with a warped extra dimension along with extensions provides the possibility for a simultaneous solution to Planck-weak hierarchy problem as well as the flavor puzzle in the Standard Model (SM). The most distinctive feature of this scenario is the existence of Kaluza-Klein (KK) gravitons whose masses and couplings to the SM fields are set by the TeV scale. In some realistic versions of this framework, the largest coupling of the gravitons to the observed particles is to the top quark and unphysical Higgses ($W_L^\pm$ and $Z_L^0$) with the KK graviton (G) masses predicted to be $\gtrsim 4 \text{ TeV}$. We extend earlier works on the KK graviton decays to the $t \bar{t}$ final state and to the “gold-plated” $Z_L Z_L$ modes (with each Z decaying to $e^+ e^-$ or to $\mu^+ \mu^-$) by studying the resonant production of the gravitons and their subsequent decay to $W_L W_L$ pair. We find that with $300 \text{ fb}^{-1}$ integrated luminosity of data the semileptonic $G \to W(\to l \nu_l) W(\to 2 \text{ jets})$ mode offers a good opportunity to search for the RS KK graviton mode with mass lighter than $\sim 3-3.5 \text{ TeV}$ at the CERN LHC. Efficient WW mass reconstruction in the semileptonic mode combined with an analysis of dilepton mass distribution in the purely leptonic channel, $pp \to W(\to l \nu_l) W(\to l' \nu_{l'})$ may help to observe KK $Z'$ and KK graviton separately. Suitably defined average energy of the charged lepton in the semileptonic mode may be used to distinguish decays from longitudinal versus transverse W-bosons.
I. INTRODUCTION

String theories inspired particle physicists to solve the problems present in the SM by introducing extra dimensions. Arkani-Hamed, Dimopolulos and Dvali (ADD) [1] proposed existence of \( n \) large extra-dimensions with factorizable geometry. In their construction SM fields are confined to our four-dimensional world. In this paper we focus instead on the Randall-Sundrum framework which uses the idea of a warped extra dimension [2]. Both scenarios predict existence of KK gravitons. Coupling of each individual ADD graviton to the SM field is suppressed by the Planck scale, but summation over almost continuous spectrum of them compensates for the suppression. RS gravitons, in contrast, have their masses and couplings at the TeV scale and therefore should appear in experiment as widely separated resonances.

The original RS model as well as all of its extensions are based on a slice of AdS\(_5\) space. At the endpoints of this five-dimensional space two branes are placed which are usually labeled as an ultraviolet (UV) brane and a Planck brane and the large hierarchy of scales is solved by a geometrical exponential factor. Postulating modest-sized 5\(^{th}\) dimension with radius \( R \) and curvature \( k \) the TeV/Planck \( \sim e^{-k \pi R} \) ratio of scales can be numerically obtained by setting \( kR \approx 11 \). If we assume that all SM fields are localized on the TeV brane, higher dimensional operators in the 5D effective theory will give large contributions to flavor changing neutral current processes and electroweak precision observables. Also to solve hierarchy in the observed fermion masses we need to have different fermion Yukawa couplings for different flavors. A natural way to accomplish this proposed by [3, 4] is to allow SM fields to propagate in the extra dimension. In this scenario light fermions are localized near the Planck brane while heavier ones near the TeV brane and, thus, the problem of fermion masses is solved since Higgs field, localized at the TeV brane will couple weakly to former and strongly to latter fermions. As a consequence, the KK graviton whose profile is peaked at the TeV brane will couple mostly to the top quark as well as to the Higgs (or, by equivalence theorem, to the longitudinal W and Z bosons) [5, 7, 8].

Thus, the promising channels to observe RS gravitons are those where produced gravitons are decaying to fields localized near the TeV brane. Search for the KK gravitons using its decays to the top quarks was performed in [5]. The 4-lepton signal through the decay to a pair of \( Z' \)'s was studied in [4]. Reconstruction possibility of the \( Z' \)'s via their leptonic decays makes this a uniquely clean mode. Both analyses concluded that with \( \sim 100\text{-}300 fb^{-1} \) of data provided by LHC the gravitons of masses up to \( \sim 2 \) TeV can be probed.

In this paper we will study purely leptonic \( G \rightarrow W_L W_L \rightarrow l \bar{l} \nu \nu \) and semileptonic modes, i.e. \((W \rightarrow l\nu)(W \rightarrow jets)\) from the decay of \( W_L \) pair. Our analysis suggests that we may be able to observe RS KK graviton mode with mass up to about \( \sim 3\text{-}3.5 \) TeV as well as to separate its contribution from that of the RS KK \( Z' \); thus, if they exist at all, providing strong evidence in favor of the RS framework [9]. Our strategy relies on the fact that in the class of models we are working \( m_1^G \approx 1.5 m_1^{Z'} \) for the lightest KK masses of the graviton and the gauge fields [31].
Thus, since $Z'$ has only $2/3$ of the graviton mass and since cross-section falls quickly as we go up in mass of the resonance being produced, we may expect that the gauge KK modes would be more accessible [10, 11, 12]. Then, by making use of the above relationship between masses, we may look for the presence of the graviton in some other mode(s) where they could be well separated. In particular, we will show that using the purely leptonic mode to observe KK $Z'$ (where graviton contribution will be hard to see due to its higher mass) we then may use the semileptonic mode with the knowledge of $Z'$ mass to pin down the graviton contribution. However, the last channel is challenging as it requires to distinguish two collimated jets from highly boosted W boson from one QCD jet. Therefore, in addition to WW irreducible SM background, we include $W + 1$ jet background in our study for this mode.

The reason for the enhancement of the graviton signal in the WW channel compared to the ZZ mode lies in the fact that the branching ratio (BR) to a $W_L$ pair is twice as big as the BR to a $Z_L$ pair. In addition to that, Br($W \rightarrow \text{hadrons}$) $\approx 2/3$ and Br($W \rightarrow l\nu$) $\approx 1/9$ compared to Br ($Z \rightarrow l^+l^-$) $\approx 3.3\%$, where $l$ indicates each type of the lepton, not sum over them [13]. Also, it is worth mentioning that a RS graviton decays to top quark pairs about $\sim 70\%$ of the time compared to $\sim 15\%$ for a $W_L$ pair. The important point for the $t\bar{t}$ final state, however, is that the KK gluon couples to the top pair as well and surpasses graviton production [10, 11]. Also, the reconstruction of such energetic tops far away from the $t\bar{t}$ production threshold might be an additional challenge.

The main experimental problem in using the WW final state with subsequent leptonic decays is the presence of one or two neutrinos. In particular, we most probably will not be able to reconstruct WW mass in the leptonic case; although this channel will be a useful discovery channel to reveal the existence of KK gauge bosons. Then, we will show that the semileptonic mode should be able to see both signals as they will be well separated due to the significant mass differences mentioned before.

To summarize, our channels allow us to probe first RS KK graviton mode with mass below 3-3.5 TeV and, also, to distinguish it from the contributions of RS spin-1 KK gauge bosons. Certainly, the full establishment of the existence of spin-2 graviton from the RS model will need combined analysis of modes discussed in this paper with other decay modes considered before in the literature [6, 7]. The role of the $Z_LZ_L$ mode is extremely important as this mode is forbidden for $Z'$'s to decay into. Note, though, that the “gold-plated” nature of this special mode, with each Z decaying to $e^+e^-$ and $\mu^+\mu^-$, comes at the price of needing a higher luminosity [9]. Thus, with the strategy discussed above and better statistics in (semi)leptonic modes of W’s, we may optimistically have evidence for the RS gravitons.

II. MODEL

We closely follow the model discussed in [7] and briefly review it here. As discussed above, we allow SM fields to propagate in the extra dimension and distribute
fermions along it to generate observed mass spectrum without introducing additional hierarchies. SM particles are identified with zero-modes of 5D fields, and the profile of the fermion in the extra dimension depends on its 5D mass. As was shown before [14, 15, 16], all fermion 5D masses are \(O(1)\) parameters with the biggest one, among the SM quarks, being that of the top quark. To specify the model even further, the top quark is localized near the TeV brane and the right-handed isospin is gauged [17]. We consider \(t_R\) being on the TeV brane (see discussion of the other possibilities in [7], for example). At the end of the day, we are left with three parameters to be measured experimentally. We define them as \(c \equiv k/M_{Pl}\) the ratio of the AdS curvature \(k\) to the Planck mass; \(\mu \equiv ke^{-\pi kR}\) which monitors gauge KK masses with the first few being \((2.45, 5.57, 8.7... )\times \mu\); and finally, parameter \(\nu \equiv m/k\), which defines where the lightest fermion with bulk mass \(m\) is localized. For the \(t_R\) on the TeV brane, \(\nu_{t_R} \approx 0.5\); and the parameters \(c\) and \(\mu\) will remain free in our analysis.

A. Low energy constraints on model parameters

We now briefly review constraints placed on the warped extra-dimension model with custodial isospin symmetry [17], which we adopt in this paper. As it was shown in [17], KK mass scale as low as \(\sim 3\) TeV is allowed by precision electroweak data. Regions of parameter space that successfully reproduce the fit to electroweak precision observables with KK excitations as light as \(\sim 3\) TeV were also studied in [18]. Implications of the observed B-mixings were discussed in [19]. In the model of [17] B-mixing is mainly accommodated by tree level exchange of KK gluons. In [19], the CP-violating effects on the \(B_d\) system were shown to provide \(M_{gluon}^{(1)} > 3.7\) TeV constraint at 68\% CL.

Phenomenological constraints from lepton-flavor-violations were discussed in [20, 21]. In [20], “anarchic” Randall-Sundrum model of flavor was studied, and the minimal allowed KK scale of \(\sim 3\) TeV was found to be permitted for a few points in the natural RS parameter space; but models with custodial isospin can relax these constraints. In [21], after extensive analysis of \(B \rightarrow K^*l^+l^-\) modes, only the \(B \rightarrow K^{*}\)ee decay was found to have sizable new physics effects. With negligible SM contributions, current experimental bounds were translated into the lepton bulk mass parameters. For the first KK gauge boson mass of 2-4 TeV, 10-20\% deviation from the SM results were found. Top quark flavor violations and B-factory signals were also studied in [22, 23, 24]. Finally, in addition to the above mentioned constraints, since these frameworks contain beyond the SM operators with \((V - A) \otimes (V + A)\) structure, they generate enhanced contributions to \(\Delta S = 2\) processes [25]. Without further flavor structure these contributions are expected to place a lower bound on the KK gluon mass of \(O(8\) TeV) [12, 26].

Actually, model building based on the underlying RS ideas continues to flourish, specially designed to find ways to lower the allowed KK-masses in face of the various experimental constraints. In fact, even a somewhat surprising claim that KK masses as low as 1 TeV, consistent with all current experimental constraints, may be found.
An interesting variant of the warped extra dimension based on 5D minimal flavor violation was recently presented in [28]. The model allows to eliminate current RS flavor and CP problem with a KK scale as low as 2 TeV. Finally, a volume-truncated version of the RS scenario called "Little Randall-Sundrum (LRS)" model was constructed in [29]. Assuming separate gauge and flavor dynamics, a number of unwanted contributions to precision electroweak, $Z\bar{b}b$, and flavor observables were shown to be suppressed in the LRS framework, compared with the corresponding RS case.

Bearing all this in mind, current theoretical constructions suggest that it would be difficult to have KK gauge bosons with masses below 3 TeV (which would imply $m_G \gtrsim 4$ TeV); if true then, as seen already in other studies [12] and will be shown here too, signals at the LHC for the RS idea would be extremely difficult to find. However, in light of the above discussion, it also seems fair to say that these models are still being developed; and, therefore, it is not inconceivable that explicit construction(s) will be found which will allow KK masses lower than 3 TeV without running into conflict with electroweak precision experiments or with flavor physics. This point of view, in particular, was also emphasized in [30]. Thus in this paper we will take the view, for now, that it is best to search for experimental signatures with the widest latitude.

**B. Couplings of KK gravitons**

After these brief remarks we can write the couplings relevant to our discussions here. Since the graviton couples to the energy-momentum tensor, all couplings have generic form $C_{00n} h_{\mu\nu} T^{\mu\nu}$ ("00n" signifies that we are considering only coupling of the nth KK graviton to the SM fields which are zero-modes of the 5D fields). Magnitude of the coupling constants depend on the overlap of the particle wavefunctions in the extra-dimension (effects of the running gravitational coupling due to existence of non-Gaussian fixed point were analyzed in [32, 33]). We present coefficients $C_{00n}$ in Table I along with partial decay widths for dominant decay channels for the lightest KK (n=1) graviton which will be the focus of our analysis; see also [7]. The $W_L W_L, Z_L Z_L$ and $hh$ decay channels illustrate equivalence theorem once again (which is valid up to $(M_W/Z/m_G)^2$ where $m_G$ is the graviton mass).

The suppression in coupling of the graviton to the gluons follows because gauge boson has a flat wavefunction and thus its couplings to the graviton is suppressed by the volume of the bulk $\pi k R \approx 35$. For the same reason, decay of gravitons to transverse W and Z bosons as well as photons are suppressed by this volume factor. The masses of the KK gravitons are given by $m_n = x_n \mu$ where $x_n$ is nth zero of the first order Bessel function. Notice that we do not need $q\bar{q}G$ coupling as it is Yukawa-suppressed and graviton production is dominated by gluon fusion.

In this model the total width of the graviton is found to be $\Gamma_G = \frac{13(c x_G)^2 m_G^3}{960\pi}$ which is split between 4 dominant decay modes to $W_L W_L, Z_L Z_L, t_R \bar{t}_R$ and $hh$ in the ratio 2:1:9:1. Taking $c \sim 1$, the total graviton width is $\sim 6\%$ of its mass and is very
TABLE I: Couplings of the nth level KK graviton to the SM fields. \( t_R \) assumed to be localized on the TeV brane. Parameter \( m_1^G \) is the mass of \( n=1 \) graviton and \( x_1^G = 3.83 \) is the first root of the first order Bessel function. \( N_c = 3 \) is number of QCD colors.

| SM fields | \( C_{00n} \) | Partial decay widths for \( n=1 \) graviton |
|-----------|-------------|-----------------------------------------------|
| \( gg(\text{gluons}) \) | \( \frac{c}{2\pi kR} \) | negligible |
| \( W_L W_L \) | \( 2c/\mu \) | \( (cx_1^G)^2 m_1^G/480\pi \) |
| \( Z_L Z_L \) | \( 2c/\mu \) | \( (cx_1^G)^2 m_1^G/960\pi \) |
| \( t_R \bar{t}_R \) | \( c/\mu \) | \( N_c (cx_1^G)^2 m_1^G/320\pi \) |
| \( h h \) | \( 2c/\mu \) | \( (cx_1^G)^2 m_1^G/960\pi \) |

close to the corresponding width for RS KK \( Z' \) in the same model [12].

III. PRODUCTION AND DECAY OF KK GRAVITONS

We are now in position to calculate the matrix element for the \( gg \to G_n \to W_L W_L \). The details can be found elsewhere [7, 34]:

\[
M(g^a g^b \to W_L W_L) = \frac{c^2}{\pi kR \mu^2} \cdot \frac{2A_{+00} \delta_{ab}}{s - (m_n^G)^2 - i\Gamma_n^G m_n^G}
\]

(1)

where, \( A_{+00} = A_{-00} = \frac{1}{2}(\hat{\beta}^2 - 2)s^2 \sin^2 \hat{\theta} \) is the only independent helicity amplitude for the decay to longitudinal W bosons. W boson velocity \( \hat{\beta}^2 = 1 - 4M_W^2/s \) and all hatted variables refer to the parton center of mass frame. We see that the amplitude has \( \sin^2 \hat{\theta} \) behavior characteristic of the \( W_L \) pair in the final state. This implies that our signal events will be concentrated in the central rapidity region, and we will exploit this fact later to separate our signal from SM background.

This amplitude gives the parton level cross-section [7]:

\[
d\sigma(gg \to W_L W_L) = \frac{|M|^2 \hat{\beta}}{512\pi s}
\]

(2)

and the proton level cross-section is obtained by convolving parton level cross-section with gluon PDF’s:

\[
\sigma(pp \to WW) = \int dx_1 dx_2 f_g(x_1, Q^2) f_g(x_2, Q^2) \hat{\sigma}(x_1 x_2 s).
\]

(3)

Note that the total cross-sections for the EW boson final states are related by \( \sigma(pp \to G \to W_L W_L) = 2 \times \sigma(pp \to G \to Z_L Z_L) \). Numerical results for our 2→2 process can be found in [2] (where the \( Z_L \) final state was used) which agrees with our current calculation.

6
IV. BATTLING SM BACKGROUND

We now discuss the relevant decay modes of the W bosons.

If both W’s decay hadronically, we face huge QCD background; and, therefore, this mode is unlikely to be useful. Thus, in the rest of this paper, we concentrate on pure leptonic and semileptonic decay modes of the W pair and consider the former first.

A. Pure leptonic mode: $e^\pm \mu^\mp$ final state

Due to the significant boost of the W’s, neutrino’s $p_T$ in this mode will be almost back to back; and, therefore, missing energy information will be lost. We require the W’s to decay to different lepton flavors since in SM there is no basic $2 \rightarrow 2$ partonic process giving two different high transverse momentum lepton flavors in the final state. After this, leading irreducible SM backgrounds for our $l^+ l^- E_T$ final state are $W^+ W^- \rightarrow l^+ l^- E_T$ and $Z/\gamma^* \rightarrow \tau^+ \tau^- \rightarrow l^+ l^- E_T$ (where $l \neq l'$).

With two neutrino’s in the final state, we might not reconstruct the resonant W boson mass. However, we will show that even looking only at the leptons (at this point by leptons we mean primarily $e$ and $\mu$; see, however, further discussion on $\tau$’s later) may provide enough data to discover the RS graviton, given a suitable set of cuts. We will show that such cuts give $S/B \gtrsim 1$ for mass of the first KK graviton mode $m_{G1} \lesssim 3$ TeV.

B. Semileptonic mode

For semileptonic channel we have highly collimated decay products for both W’s. For the hadronic side, it implies that the two jets from the W decay are likely to appear as one “fat” W-jet. This leads us to consider W + 1 jet which will be the leading background for this decay mode compared to irreducible SM WW production and W + 2 jets (which will be suppressed due to the 3 body phase-space). On the leptonic side, due to small angular separation between missing neutrino and charged lepton, we may estimate longitudinal (L) component of the $\nu$’s momentum as

$$p_{\nu}^L \approx \frac{E_T p_T^L}{p_T^\nu}.$$  \hspace{1cm} (4)

Using this collinear approximation, the momentum of the leptonic W is reconstructed and, thus, we can calculate the (presumably) resonant invariant mass of the semileptonic system as $M_{WW}^2 = (p_{\nu} + p_{jj})^2$. Notice that we assumed that leptons are coming from the W decay as the reconstructed leptonic W mass will be zero in the collinear approximation. Also notice that in this approximation, the $M_{WW}$ measurement error for the TeV energy W bosons is $\sim m_W/E_W \sim 0.1$. The accuracy of this invariant mass measurement will also depend on how effectively hadronic W
side can be reconstructed. We will elaborate on this at the beginning of section \textbf{V} B.

\section{Acceptance Cuts and Results}

We now present our results as well as specify selection criteria for signal events. We estimated SM background with the aid of the COMPHEP package \cite{35}. For our graviton signal we used Mathematica program and partially cross-checked them with COMPHEP. For an additional check, we confirmed results of Ref.\cite{7} for $\sigma(pp \rightarrow G \rightarrow Z_LZ_L)$, as was mentioned before. The CTEQ5M PDF’s were used throughout (in their Mathematica distribution package \cite{36} as well as intrinsically called by COMPHEP).

\subsection{Pure leptonic mode: $e^{\pm}\mu^{\mp}$ final state}

As a starting point, before imposing any cuts, we reproduced results of Ref.\cite{37} which finds $\sigma(pp \rightarrow e^+\nu_e\mu^-\bar{\nu}_\mu) \approx 610$ fb and is dominated by WW production. We cross-checked our WW production results with Ref.\cite{12} as well.

We impose basic acceptance cuts as

$$|\eta_l| < 3, \quad p_{T_l} > 50 \text{GeV}, \quad \mathbb{E}_T > 50 \text{GeV},$$

where $\eta_l$ is the pseudorapidity of the charged lepton.

In Fig.\textbf{1}a,b we show the total cross-section for $pp \rightarrow l\nu_l l'\bar{\nu}_{l'}$ (where $l \neq l'$) and expected number of events per 300 fb$^{-1}$ as a function of $m_G$ for our signal. The corresponding SM background is $\approx 24$ fb and is dominated by the WW production with contribution from $Z/\gamma^* \rightarrow \tau^+\tau^- \rightarrow l^+l^- \mathbb{E}_T$ process being about an order of magnitude smaller, which also is in good agreement with corresponding results of Ref.\cite{12}.

We see that as the SM background dominates, we need to look for additional cuts to improve signal observability. Invariant dilepton mass may provide additional information to enhance our S/B ratio. In Fig.\textbf{2} we show dilepton invariant mass distributions for signal and corresponding background where $m_G = 2$ TeV and 3 TeV values were chosen.

We observe that the SM background distributions tend to peak at low dilepton invariant mass while signal events concentrate in the middle mass region dictated by the decay of the very massive object. This allows us to define cuts on dilepton mass. For the masses shown on Fig.\textbf{2} for example, we have chosen them as

$$m_G = 2 \text{ TeV} : \quad m_{ll'} > 1 \text{ TeV}$$
$$m_G = 3 \text{ TeV} : \quad m_{ll'} > 1.5 \text{ TeV}$$

(6)
to improve the statistical significance of the signal further. Table I shows the statistical results after all the cuts defined above were applied. We notice that the SM background was reduced significantly while the signal was roughly reduced by half. Throughout the paper, Poisson statistics CL to observe at least one signal event will be appropriate description if the number of background events is \( \lesssim 10 \). When needed, these CL are given in brackets next to the corresponding statistical significances in Gaussian statistics.

In the model we are working, there will also be a contribution to the signal from the KK \( Z' \). If we use the mass ratio of this model \( m_1^G \approx 1.5 m_1^{Z'} \), we observe, for example, that a 3 TeV graviton should appear along with a 2 TeV \( Z' \). Interestingly, we find that the total production cross-section for 2 TeV graviton and \( Z' \) are very
similar in magnitude (it is about 16 fb for $Z'$ [12] compared to 10 fb for graviton) and shape. Thus, 2 TeV graviton contribution in Fig. 2 may be numerically viewed as the one coming from $Z'$. After this observation, Fig. 2 represents signal cross-section for 3 TeV graviton along with SM background and 2 TeV RS $Z'$. Similarly for 2 TeV graviton, 1.33 TeV $Z'$ needs to be considered and so on. As two contributions are mixed up in this channel, it might be easier to “reserve” this channel for $Z'$, since corresponding graviton contribution will be negligible. Stated differently, if enhancement in dilepton mass due to these states will be observed experimentally, most probably $Z'$ will have a dominant effect. Then, Fig. 2 may be used to define a proper cut on dilepton mass variable to remove this $Z'$ background (for example, for 3 TeV graviton $m_{ll} > 2$ TeV will work). Of course, it might happen that the lightest KK $Z'$ and graviton masses are actually in different ratio; and we need other measurement(s) to interpret enhancement in dilepton mass. In the next section we will show that semileptonic mode may provide this additional handle.

B. Semileptonic decay

As discussed above, leptonic W momentum for this mode can be reconstructed; and W + 1 jet is a leading background. As in the case of the leptonic mode, we define basic selection cuts as

$$|\eta_{l,j}| < 1, \quad p_{T_l} > 50 GeV, \quad E_T > 50 GeV, \quad p_{T_j} > 100 GeV; \quad (7)$$

and in Fig. 3 we show the expected number of signal and background events, both integrated over one half of the graviton width. Assuming again that $m_G \approx 1.5m_{Z'}$,
TABLE II: Purely leptonic mode cross-sections [in fb] and S/B ratios after basic and
dilepton mass cuts in Eq.5 and Eq.6 were imposed. When the number of events is low
(\lesssim 10), Poisson statistics confidence level is considered a more appropriate statistical
description and is consequently used.

| Energy (TeV) | Basic cuts | Dilepton mass cut | # of events/300 fb\(^{-1}\) | S/B   | S/\sqrt{B} |
|-------------|------------|-------------------|-----------------------------|-------|------------|
| 2           | Signal     | 0.22              | 0.1                         | 30    | 2.5        | 8.7        |
|             | Background | 24                | 0.04                        | 12    |            |            |
| 3           | Signal     | 0.0087            | 0.004                       | 1.2   | 0.6        | 0.8 (64\%) |
|             | Background | 24                | 0.007                       | 2.1   |            |            |

the Z' contribution is negligible in this WW invariant mass window because Z' and
graviton total widths are \sim 5\% of their mass, while the mass difference between Z' and
graviton is \sim 50\% of Z' mass; this also assumes that the Z' mass is established
by the pure leptonic mode.

FIG. 3: The total signal (solid) and SM background W + 1 jet (dotted) cross-section
(integrated in \(m_G \pm \Gamma_G/2\) window) after cuts specified in Eq.7 were applied.

We see that the background is severe; and, therefore, its reduction is a serious
and challenging issue. One quantity that may help to resolve the problem is a jet-
mass, which is the combined mass of the vector sum of 4-momenta of all hadrons
making up the jet. For the signal, we expect jet-mass to peak at \(M_W\). Along these
lines, as it was shown in Ref.\[12\], the cut on the jet-mass \(75 < M_{jet} < 125 \text{ GeV}\) gives
a substantial rejection of the background events (\approx 70\%) while accepting most of
the signal. Also, EM calorimeter, due to its finer segmentation, may allow to improve
jet-mass resolution, since signal W events are expected to have two separated EM cores. For further discussion on this issue, we refer to Ref. [12, 38, 39, 40].

In an attempt to specify the selection cuts further, in Fig.4 (note that the scale is linear) we show the lepton energy distribution for graviton masses $m_G = 2 \, \text{TeV}$ and $m_G = 3.5 \, \text{TeV}$ for the same conditions as in Fig.3. We observe that by defining appropriate cuts on lepton energy signal observability can be improved. We define them as

$$m_G = 2 \, \text{TeV} : \quad 0.2 \, \text{TeV} < E_{\text{lepton}} < 1 \, \text{TeV}$$
$$m_G = 3.5 \, \text{TeV} : \quad 0.5 \, \text{TeV} < E_{\text{lepton}} < 1.4 \, \text{TeV}$$

and show resulting statistics in Table III. We observe that with 300 fb$^{-1}$, it is possible to reach 1$\sigma$ effect for 3.5 TeV graviton.

With efficient hadronic W mass reconstruction, we have another case when most of the hadronic QCD background can be separated; and we are left with WW as the only irreducible background. Fig.5 shows results for this situation with $c \equiv k/M_{Pl} = 1$ and 2 (see Ref.[7] for the discussion of the range of c). Notice that for Fig.5 we integrated over $(m_G \pm \Gamma_G)$ WW invariant mass window compared with $(m_G \pm \Gamma_G/2)$ window for Fig.3.

We see that in the $c=1(2)$ case, gravitons up to 3.5 TeV (4 TeV) mass might have enough events to be observed with good statistical significance; see Table III. Dependence of the SM WW background on the c value follows from the fact that $m_G \pm \Gamma_G$ integration region is not constant since $\Gamma_G \sim c^2$.

In parallel with leptonic mode, we need to remember that we have a neutral gauge bosons $Z'$ produced (through $q \bar{q}$ annihilation or vector boson fusion processes) which might consequently decay to $W_L$ pair [12]. Using $m_{i_1}^G \approx 1.5 m_{i_1}^{Z'}$, in Fig.6 we show that for 2 TeV $Z'$ and corresponding $\sim 3$ TeV graviton, the signals are well separated as a function of reconstructed WW invariant mass. Thus, by putting a $M_{WW} > 3 \, \text{TeV}$ cut, the $Z'$ signal will become negligible and enhancement in total cross-section is due to graviton only (we obtained graviton cross-section to be 0.04 fb after $M_{WW} > 3 \, \text{TeV}$ cut). Now, 2 TeV $Z'$ can be discovered with 5$\sigma$ statistical significance for an integrated luminosity of 100 fb$^{-1}$ in purely leptonic channel as was shown in [12], and there the 3 TeV RS graviton contribution will be negligible. Thus, assuming that $W + 1$ jet background will be manageable (for example, by means discussed above) and $Z'$ mass is estimated from some other mode (from purely leptonic one we considered above, for example) we may expect to confirm existence of RS graviton in semileptonic channel. Clearly, even if the above relation between masses of these lightest KK modes will not turn out to be true or some other resonance(s) will appear in this channel, WW mass spectrum measurement should still provide an important additional information.
FIG. 4: Differential lepton energy distribution for the signal (solid) and SM $W + 1$ jet background (dotted) (integrated in $m_G \pm \Gamma_G/2$ window) after cuts specified in Eq.7 were applied for (a) $m_G=2$ TeV and (b) $m_G=3.5$ TeV.

VI. DISCUSSION

We saw in previous sections that (semi) leptonic modes from $W_L$ pair decay have a potential to discover RS graviton up to about (3.5 TeV) 3 TeV of mass. To increase statistics, we might expect to use $\tau$ leptons which will give us combinatorial factor of 3 and 3/2 for leptonic and semileptonic modes respectively from additional decay channels; therefore, the inclusion of the $\tau$’s can help appreciably. The reason for optimism on the issue of the detection of the $\tau$’s is that $\sim$500 GeV energy $\tau$’s have a decay length of $l = \gamma \tau c \approx 20$ mm and, thus, might leave visible tracks in the detector [41]. For $m_G \gtrsim 3.5$ TeV, higher luminosities are required which will scale our results accordingly [42]. Similarly, upgrades of the center of mass energy
FIG. 5: (Color online) (a) The total signal (solid) and SM background (dashed) cross-section (integrated in $m_G \pm \Gamma_G$ window) for $pp \rightarrow W(l\nu)W(jj)$ after $|\eta_W| < 1$ cuts were applied for c=1 (red) and c=2 (blue) values, (b) Corresponding number of events for 300 fb$^{-1}$.

at LHC [43] can extend the reach in KK mass.

So far, the study of the RS gravitons was based either on the total cross-section or reconstructed graviton mass measurements. We might try to exploit unique spin-2 nature of the graviton, which might be challenging in our channels. For example, one might be tempted to use lepton pseudorapidity which, due to the high boost of the decaying $W$’s, will be $\sim \sin^2 \theta$ behavior of the basic 2→2 underlying scattering process. But high-energy $W_L^+W_L^-$ production in the SM and RS $Z'$ decaying to two $W_L$ also have this behavior and, thus, will be indistinguishable in shape from our signal.

Also, we might use information on lepton energy to establish that $W$’s from
TABLE III: Semileptonic mode signal cross-sections [in fb] and S/B ratios along with W + 1 jet and WW SM backgrounds. Signal 1 and the corresponding W + 1 jet background results were obtained after cuts in Eqs. were imposed and mg ± Γ/2 integration region was chosen. Signal 2 and corresponding WW background results were obtained after |ηW| < 1 cut and integrated in mg ± Γ window. When the number of events is low (≤ 10), Poisson statistics confidence level is considered a more appropriate statistical description and is consequently used.

| Cuts                  | # of events/300 fb⁻¹ | S/B   | S/√B  |
|-----------------------|-----------------------|-------|-------|
| 2 TeV                 |                       |       |       |
| Signal 1 [c=1]        | 1.7                   | 510   | 1.04  | 23    |
| W + 1 jet background  | 1.64                  | 492   |       |       |
| Signal 2 [c=1]        | 2.0                   | 600   | 13.3  | 90    |
| WW background [c=1]   | 0.15                  | 45    |       |       |
| Signal 2 [c=2]        | 7.8                   | 2340  | 7.8   | 135   |
| WW background [c=2]   | 1.0                   | 300   |       |       |

| 3.5 TeV               |                       |       |       |
| Signal 1 [c=1]        | 0.01                  | 3     | 0.33  | 1 (54% ) |
| W + 1 jet background  | 0.03                  | 9     |       |       |
| Signal 2 [c=1]        | 0.02                  | 6     | 2.9   | 4.1 (99% ) |
| WW background [c=1]   | 0.007                 | 2.1   |       |       |
| Signal 2 [c=2]        | 0.07                  | 21    | 1.4   | 5.4   |
| WW background [c=2]   | 0.05                  | 15    |       |       |

our graviton decay are longitudinally polarized. This analysis is most promising in semileptonic mode because, as discussed in section IV B, in this mode WW mass can be reconstructed. Leptons from W_L decay will be preferentially emitted in the direction of the spin axis which is perpendicular to the direction of W motion. Thus, lepton and neutrino will tend to have the same energy in the lab frame, compared to decay of transversely polarized W’s where they are emitted in the direction of the W motion and, thus, one of the W decay products will carry most of the energy. Now, suppose we have a negatively charged W decay. To confirm that W’s from our graviton decay are longitudinally polarized, we calculated the average lepton energy in the lab frame from the decay of polarized W bosons and summarized our results in Table IV. We notice that the average for the longitudinally and transversely polarized W’s (which is the average of left-handed and right-handed polarizations) is the same and equal to \(\sqrt{s}/4\). To distinguish between longitudinal and transverse polarizations, we divide signal events into two groups: events in the first group will have charged lepton energy bigger than the neutrino’s energy; and in the second group, the neutrino’s energy will be bigger. The fact that lepton’s energy is bigger (smaller) implies that lepton’s 3-momentum in the W rest frame is parallel (antiparallel) to W’s 3-momentum in the lab frame. We calculated the average lepton energy in the lab frame from the decay of polarized W bosons for the
FIG. 6: Contributions of the 2 TeV gauge boson and 3 TeV graviton to the $pp \rightarrow W(l\nu)W(jj)$ process. Cuts specified in Eq.7 were applied and $c=1$.

TABLE IV: Average lepton energies in the lab frame from the decay of polarized $W^-$ bosons. For a $W^+$ decay, the results for the left-handed and right-handed rows need to be switched.

| $W$ polarization | Average | Average for group 1 | Average for group 2 |
|------------------|---------|---------------------|---------------------|
| Longitudinal     | $\sqrt{s}/4$ | $(8 + 3\beta)\sqrt{s}/32$ | $(8 - 3\beta)\sqrt{s}/32$ |
| Left-handed      | $(2 + \beta)\sqrt{s}/8$ | $(28 + 17\beta)\sqrt{s}/112$ | $(28 - 17\beta)\sqrt{s}/112$ |
| Right-handed     | $(2 - \beta)\sqrt{s}/8$ | $(28 + 17\beta)\sqrt{s}/112$ | $(28 - 17\beta)\sqrt{s}/112$ |

events in each group and presented our results in Table IV as well. We see that this analysis could be used to confirm that $W$'s from our graviton decay are longitudinally polarized as, presumably, average lepton energies will match the $(8 + 3\beta)\sqrt{s}/32$ and $(8 - 3\beta)\sqrt{s}/32$ values for the signal events in the first and second group respectively. For a positively charged $W$ decay, the results for the left-handed and right-handed rows in Table IV need to be switched.

VII. CONCLUSION

In this work, we have extended earlier studies of the discovery potential of warped gravitons at the LHC which concentrated on the gravitons decaying into the “gold-plated” ZZ channel and into the $t\bar{t}$ pair. We have considered resonant production of the first RS KK graviton mode via gluon-fusion process followed by its subsequent decay to $W_LW_L$ pair. We focused on leptonic and semileptonic final
states and found that with $300 fb^{-1}$ of data, LHC may discover first RS KK graviton with masses below $\sim 3$ TeV and 3.5 TeV in these modes respectively. We also incorporated potential KK $Z'$ signal in both modes and analyzed its combined effect with RS graviton. Taking the RS prediction for the lightest KK masses, $m_G^1 \approx 1.5 m_{Z'}^1$, we showed that these signals are well separated in reconstructed WW invariant mass in the semileptonic mode. For the purely leptonic $e\mu$ mode, where resonance mass reconstruction is problematic, the above mass relationship hints to the domination of the $Z'$ events as corresponding graviton mass will be higher. Nevertheless, we demonstrated that even in that mode, appropriate choice of cuts in dilepton invariant mass may be able to distinguish these contributions as well.

Acknowledgments

We thank H. Davoudiasl for a careful reading of the manuscript and to him and to J. Cochran for useful discussions. O.A. also would like to thank BNL Physics Department for hospitality during part of this project. Work of O.A. and D.A. are supported in part by DOE under contract number DE-FG02-01ER41155. A.S. is supported in part by the DOE grant DE-AC02-98CH10886 (BNL).

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In all the numerical estimates presented in this paper, we will only include $W \rightarrow e\nu_e$ and $W \rightarrow \mu\nu_\mu$. However, towards the end in Section VI we will emphasize that the detection of the $\tau$'s from these decays may indeed be feasible.

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