Dynamics of the Ethanolamine Glycerophospholipid Remodeling Network

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Abstract

Acyl chain remodeling in lipids is a critical biochemical process that plays a central role in disease. However, remodeling remains poorly understood, despite massive increases in lipidomic data. In this work, we determine the dynamic network of ethanolamine glycerophospholipid (PE) remodeling, using data from pulse-chase experiments and a novel bioinformatic network inference approach. The model uses a set of ordinary differential equations based on the assumptions that (1) sn1 and sn2 acyl positions are independently remodeled; (2) remodeling reaction rates are constant over time; and (3) acyl donor concentrations are constant. We use a novel fast and accurate two-step algorithm to automatically infer model parameters and their values. This is the first such method applicable to dynamic phospholipid lipidomic data. Our inference procedure closely fits experimental measurements and shows strong cross-validation across six independent experiments with distinct deuterium-labeled PE precursors, demonstrating the validity of our assumptions. In contrast, fits of randomized data or fits using random model parameters are worse. A key outcome is that we are able to robustly distinguish deacylation and reacylation kinetics of individual acyl chain types at the sn1 and sn2 positions, explaining the established prevalence of saturated and unsaturated chains in the respective positions. The present study thus demonstrates that dynamic acyl chain remodeling processes can be reliably determined from dynamic lipidomic data.

Introduction

Lipids are fundamental building blocks of cellular membranes and are also essential for signal transduction, energy homeostasis, and many other cellular processes. Recent advances in mass-spectrometry have made large-scale quantification of lipidomes possible [1,2] and have revealed an unprecedented diversity of lipid species [3–5]. Such lipidomics data provide an enormous amount of information, which should eventually lead to understanding of the mechanisms underlying lipid homeostasis and its impact on cellular functions.

Glycerophospholipids are the dominant lipids in mammalian membranes and are comprised of a glycerol moiety, a polar head group linked via a phosphate to the sn3 position of the glycerol moiety as well as an acyl chain esterified to the sn1 and the sn2 positions [6]. The hydrocarbon chain in the sn1-position can also be linked to the glycerol moiety via an alkyl or alkylol ether bond. Because of these variations as well as the variation of the length and number of double bonds, glycerophospholipids comprise a great number of molecular species. The molecular species composition is regulated by biosynthesis, turnover and acyl chain remodeling (i.e. the Land’s cycle [7]), mediated by phospholipases and acyltransferases or transacylases. Distortions of the molecular species distributions can lead to severe pathophysiological consequences and altered lipid distributions have been found in many diseases such as Barth Syndrome, heart failure, type 2 diabetes, and several types of cancer [8–12]. Understanding of these distortions is a crucial problem, for cell and developmental biology, potential diagnostics and treatments, and nutrition [13]. The mechanisms by which lipid composition influences human diseases in most cases remain to be elucidated, though lipids have common roles in membrane structure, membrane trafficking, regulation of membrane proteins, and cellular architecture [13]. For example, it was recently shown that obesity increases arachidonic acid in membrane phospholipids, and that subsequent lipid remodeling retargets arachidonic acid to ether lipids. This process is believed to make adipocytes more vulnerable to inflammation [14].

Traditionally, the acyl remodeling process has been studied by addressing the specificity of individual enzymes in vitro using a limited number of substrate species [15–18]. The recent advances in lipidomics suggest that deeper understanding could be obtained...
by applying novel data-mining approaches to lipidomic data, but it remains a challenge to accurately infer the remodeling processes from these complex datasets. Some aspects of acyl remodeling have been revealed by computational approaches. For example, the molecular species composition of cardiolipin can be closely fit by a model in which the four cardiolipin acyl chains are remodeled independently and identically [11,19,20]. But the picture is incomplete as the fit breaks down in the case of cancerous tissues and may also be distorted by cell culture conditions [19]. Pulse-chase time course experiments [21,22] would be superior for determining remodeling mechanisms, but currently there are no computational methods to infer the processes and their associated kinetic parameters from lipid time course data.

In particular, pulse-chase experiments with isotope-labeled precursors (such as choline or ethanolamine) should provide superior information to steadystate measurements [23–25], but the interpretation of pulse-chase experiments is complicated by simultaneous labeling of a multitude of molecular species already during the pulse. To avoid this complication, we recently devised a novel approach that allows one to study metabolism of individual phospholipid species in unprecedented detail [21]. A multitude of PE or PS species with a deuterium-labeled head group were synthesized and introduced to cultured cells using cyclodextrin-mediated transfer, and the metabolism of the species in time was monitored by electrospray ionization mass spectrometry. While the PE and PS species similar or identical to endogenous species were hardly remodeled (as expected), those not present endogenously were rapidly remodeled at both the sn1 and sn2 position, eventually yielding a molecular species profile similar to that of the endogenous PE and PS. Major differences in remodeling pathways and kinetics were observed between the species within a class, as well as between corresponding PE and PS species. However, due to complexity of the data, the contributions of the alternative remodeling pathways could be only roughly estimated.

To more effectively analyze this type of data, we have now constructed a novel predictive method for determining the lipid remodeling network and its parameter values. We demonstrate the usefulness of this approach by analyzing data from pulse-chase experiments with 6 different exogenous phosphatidylethanolamine precursors, i.e. 14:0-14:0, 14:1-14:1, 18:3-18:3, 18:0-18:1, 18:1-18:1, 18:0-22:6 [21].

**Results**

Our model assumes that (1) sn1 and sn2 acyl positions are independently remodeled, (2) remodeling reaction rates do not vary over time and (3) the concentrations of the acyl donors are constant. These assumptions, which are based on previous findings on acyl remodeling of phosphatidylethanolamine, phosphatidylcholine and cardiolipin [19,20,26], allowed us to model the system using a simplified framework with a small number of parameters. We have developed a two-step algorithm to automatically determine and solve for key remodeling parameters. This algorithm consists of a flux analysis step to construct and simplify the remodeling network, followed by a B-spline-based parameter inference step that optimally solves the ordinary differential equations governing the system.

We analyzed a set of 6 separate pulse-chase experiments carried out previously (see Methods and [21]). In those experiments exogenous PE species with a deuterium-labeled head group were introduced to BHK21 cells for 1 hour using a cyclodextrin carrier and the cells were then chased for 24 h. During the chase, a number of new PE species were generated due to extensive acyl remodeling as revealed by ESI-MS analysis. The exogenous PE precursors studied were 14:0-14:0, 14:1-14:1, 18:3-18:3, 18:0-22:6, 18:0-18:1 and 18:1-18:1. The data for each of these experiments were analyzed using a two-step procedure outlined in Figure 1. In this procedure, data from individual pulse chase experiments are used for (1) network inference of acyl remodeling reactions and (2) inference of parameter values for these reactions.

**Inference of the remodeling correlation network**

We consider the PE remodeling system as a chemical reaction network, defined by a finite directed graph $G = (V, E)$, where $V$ is the set of vertices consisting of PE molecular species, $S = \{S_1, S_2, \ldots, S_n\}$, and $E$ is the set of edges, each representing a remodeling reaction converting source species to target species. Each edge associates with a remodeling reaction rate that depends on the remodeled chain only. Here we use the sn1 and sn2 position independence assumption [26] so that any two connected PE species differ at only one position. Figure 2 (A) shows the full remodeling network for the 18:3-18:3 PE precursor. There can be up to $n_1 n_2 (n_1 + n_2 - 2)$ edges in the full network where $n_1$ and $n_2$ represent the number of sn1 and sn2 chain types, though in practice we do not count edges to PE species that are not experimentally observed as part of the full network. Parameter inference on the full network of interactions would be very slow and is likely to lead to over-fitting.

Remodeling in cells is likely to proceed primarily through a subset of the possible edges in the full network. The first step toward the identification of the dominant remodeling pathways was taken in ref. [21], where the unimportant edges in the full network were eliminated by manually examining the changes in PE species concentrations over time. Here, we extend and automate this process using a fast and accurate correlation network algorithm that reduces the complexity of the full network. Briefly, the algorithm iteratively cycles through candidate “source” and “target” species and examines whether the concentration of the source species is inversely correlated to the sum of the concentrations of the target species. The significance of each connection is calculated using a standard t-test, which can be used to set a threshold for connections. Figure 2 (B) shows the output of the algorithm for the 18:3-18:3 precursor experiment (threshold significance level $p = 0.3$) including correlation score and the evidence time interval for each connection. We observed that results are relatively insensitive to the choice of significance level (See Methods).

Figure 2 (C) shows the reduced bidirectional correlation network for the 18:3-18:3 precursor experiment (See Supporting Information S1 for results for the other precursors). As can be seen, a large component of the flux involves the conversion of 18:3-18:3 to 18:1-18:3 and the conversion of the latter to 18:1-18:1. This suggests that remodeling of 18:3 at the sn1 position is faster than at the sn2 position. Similarly, in the 14:1-14:1 precursor experiment, the 14:1-14:1 precursor is first converted at the sn1 position to become 18:1-14:1 and then at the sn2 to become 18:1-18:1 (Supporting Information S1). However, the major path of the 14:0-14:0 experiment differs (Supporting Information S1). 14:0-14:0 is first converted at the sn2 to become 14:0-18:1 and then to 18:1-18:1. An open question is whether the remodeling mechanisms can still be the same in these experiments, and how the apparent differences in sn1 and sn2 ordering can be explained. These points will be addressed below.

**Dynamic simulation**

Once a correlation network has been inferred for a given experimental timecourse, the behavior of the system can be forward simulated using ordinary differential equations (ODEs)
determined by the reduced bidirectional correlation network. Table 1 shows the dynamical system governing the 18:3-18:3 experiment reactions (See Figure 2 (C) for a graph of the network).

To infer the values of the parameters in the correlation network, we implemented an expectation-maximization-like B-Spline algorithm in which parameter values are updated iteratively to minimize an objective error function [27] subject to the constraint that the solution satisfies the ODEs that govern the system (See Methods).

Figure 2. Full PE remodeling network and reduced network based on flux analysis. The full PE remodeling network of 18:3-18:3 pulse-chase experiment consists of all possible acyl chain exchange reactions between lipid species at any time t, assuming sn1 and sn2 positions are independently remodeled (A). The simpler remodeling network (C) inferred from flux analysis (B) can be adequate for fast and accurate determination of the system. Flux analysis identified reactions with significant evidence that one species converts to the other. A large portion of flux in (B) involves 18:3-18:3 converted to 18:1-18:3 and then converted to 18:1-18:1, according to the edge correlation score (Equation 2) and evidence time range in brackets.

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Table 1. Differential equation model for PE dynamic remodeling.

| Reaction                                    | Production from other species | Conversion to other species |
|---------------------------------------------|------------------------------|-----------------------------|
| $d[18:3-18:3] \frac{d}{dt}$                | $k_5[18:0-18:3]+k_1[18:1-18:3]+k_4[16:1-18:3]$ | $-k_2[18:3-18:3]-k_2[18:3-18:3] - k_4[18:3-18:3]$ |
| $d[18:1-18:1] \frac{d}{dt}$                | $k_1[18:1-18:3]$                        | $-k_1[18:1-18:1]$            |
| $d[18:0-18:3] \frac{d}{dt}$                | $k_2[18:3-18:3]+k_1[16:1-18:1]$          | $-k_1[16:1-18:3]-k_1[16:1-18:3]$ |
| $d[18:0-16:1] \frac{d}{dt}$                | $-k_1[18:1-18:3]$                      | $-k_1[18:0-18:3]$            |
| $d[14:0-18:3] \frac{d}{dt}$                | $k_1[18:1-18:3]$                        | $-k_1[18:1-18:1]$            |
| $d[14:0-18:1] \frac{d}{dt}$                | $k_2[18:3-18:3]+k_1[18:1-18:1]$          | $-k_1[18:1-18:3]-k_1[18:1-18:3]$ |

Shown are the ODEs for the 18:3-18:3 remodeling system, according to the correlation network in Figure 2 (C). The reaction parameters $k$ are unknown a priori. They depend on the sn1/sn2 position, initial chain type, and product chain type.

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Figure 3 shows the fit results for each of the six experiments. For these datasets, we observed that parameter values generally converged within 1000 iterations (See Supporting Information S1). As can be seen, the simulation curves closely fit the experimental data, suggesting that the models accurately describe the PE remodeling system. As a control, we repeated the inference procedure on nonsense data generated by permuting labels on the experimental data 100 times and compared the quality of the fit to that found for the real data. We performed random label permuting of the data 100 iterations (See Supporting Information S1). As can be seen, the simulation curves closely fit the experimental data, suggesting that the models accurately describe the PE remodeling system. For each experiment except the 18:0-18:1 precursor experiment we performed random label permuting of the data 100 times and compared the quality of the fit to that found for the real data. The 18:0-18:1 precursor experiment was not used because the original data contains only 2 lipid species. For three of the experiments (14:0-14:0, 14:1-14:1, 18:3-18:3) we observe that the real data is systematically better fit by our procedure than the permuted datasets, as shown in Figure 5 (left). The mean and standard deviation of the error function are shown across 100 permutations for each of the experimental sets. The fit error for the real data is also lower than the average error for the 18:0-22:6 and 18:1-18:1 experiments, though this effect is weaker than for the other experiments.

In addition, we observed that fits were systematically worse when we used parameters other than those that were found in the correlation network inference step. We observed that when we removed the parameters corresponding to the major reactions (sn1 precursor to 18:1) and (sn2 precursor to 18:1) and added in random parameters to replace them, the fit procedure converged on worse error values. This is shown in Figure 5 (right). These findings demonstrate that the close fits for the real data were not due to overfitting. We note also that it is important to use bidirectional reactions rather than only the 1-way processes observed in the network inference step (See Supporting Information S1). A list of all inferred parameters in all experiments is given in Supporting Information S1.

Decaylation and reacylation at sn1

Since the same cell line is used in all experiments, we hypothesized that the inferred remodeling parameters should be the same in all experiments, and if so this would support the accuracy of our inference procedure. Primary conversions, i.e. those involving acyl flux from an acyl chain found in the PE precursor, should have the most reliable inferred parameter values. This is due to their high initial abundance in each experiment and the large changes in the precursor concentration over time. Therefore we focused on comparisons of the primary effect parameter values across the experiments. Table 2 shows the primary effect parameter values inferred in each experiment.

Remarkably, the individually solved remodeling mechanisms from the six experiments show strong consistencies, suggesting that our model correctly describes the behavior of the biological system. For example, the sn1 18:0 to 18:1 conversion rates inferred from the two precursor experiments (18:0-22:6 and 18:0-18:1) are consistent (0.0673 and 0.07 respectively). While conversion rates were dependent on the initial chain and the new chain, we observed certain regularities. For example, chains convert at varying rates to 18:1 at the sn1 position. The fastest converting chain is 14:1 and the slowest is 18:0, with overall order 14:1 > 18:3 > 14:0 > 18:0 (relative rates 0.5903, 0.2500, 0.0899, 0.07). Since all of these chains are being converted to the same product, rates must differ because of differences in deacylation rate. 14:1 is the most rapidly deacylated sn1 chain while 18:0 is the one most slowly deacylated. Analogously, when we examined the rates associated with conversion to 18:0 at the sn1 position, we saw that 14:1 deacylated the fastest, just as we saw that 14:1 deacylated the fastest in conversions to 18:1. In fact, the 18:1 column and the 18:0 column both have (14:1, 18:3, and 14:0) as their three fastest reactions, respectively). While conversion rates

We observed a similar effect with reacylation. To determine whether the reacylation rate is also dependent on the chain type, we examined the relative rates of sn1 chain conversion to 18:1, 18:0 and 16:1. For the 14:0-14:0, 14:1-14:1, and 18:3-18:3 PE precursors, the ratios of the conversion rates of the sn1 precursor to 18:1, 18:0 and 16:1 were 1 : 0.1 : 0.29, 1 : 0.18 : (no data), and 1 : 0.26 : 0.24, respectively. Thus these ratios are relatively robust. (Normalization by the precursor-to-18:1 rate is necessary to account for differences in the deacylation rate of the precursors) This behavior indicates that common mechanisms are active in separate precursor experiments. Therefore, cross-validation using independent precursors should be generally effective for determining model robustness. The observed consistency of rates also indicates the accuracy of our methodology.
More generally, we were able to distinguish deacylation and reacylation rates and determine relative rates for different chain types by integrative analysis of the combined data using the steady state approximation for the concentrations of reaction intermediates (See Methods). For example, by normalizing the fitted sn1 kinetic parameters in Table 2 to 18:1, which is the fastest converted chain type, we obtain that on average, the sn1 reacylation rates have the order 18:1 > 16:1 > 18:0 (1:0.27:0.21 – see Supporting Information S1). Reacylation rates are controlled by the abundance of the given chain type in the donor lipid pool, and selectivity is determined by the acyltransferases/ transacylases involved. We observe that the deacylation rates decrease in the order 14:1 > 16:3 > 14:0 > 18:0 > 18:1 (1:0.46:0.15:0.12:0.03 – see Supporting Information S1), reflecting the specificity of phospholipase A1. Thus unsaturated chains are removed faster from the sn1 position than saturated ones, which at least in part explains why saturated chain types are enriched at sn1. Consistent with our previous suggestion [21], removal of 18:1 from the sn1 position is considerably slower than that of other acyls such as 14:0 and 18:3. For more detail on calculation of

![Figure 3. Fit of dynamic simulations for six pulse-chase experiments. Precursors are 14:0-14:0 (A), 14:1-14:1 (B), 18:3-18:3 (C), 18:0-22:6 (D), 18:0-18:1 (E) and 18:1-18:1 (F). Simulations (curve) are in good quantitative agreement with measurements (dots and bars indicate mean and standard error of the mean across replicates). The errors (Equation 8) between prediction and observation are 387, 1064, 2680, 753, 262, and 118 respectively. doi:10.1371/journal.pone.0050858.g003](image1)

![Figure 4. Permutation test result. To examine the robustness of the model, we randomly permuted species labels of the data and used them to solve dynamic system defined by the original data. Shown here are results for the 18:3-18:3 (a) and 14:0-14:0 (b) experiments as examples. As can be seen, the fitting performances are much worse than for the original data, with larger error 5221 compared to original 2680 (a) and 458 compared to original 387 (b). The curves are simulations and the dots are randomly permuted data. doi:10.1371/journal.pone.0050858.g004](image2)
Deacylation and reacylation rates, see Method and Supporting Information S1.

Deacylation and reacylation at sn2

Robust deacylation and reacylation rates were also found for the sn2 position, although there were less data than for the sn1 position. For example, the relative conversion rate of 14:0 to 18:1 vs. 18:2 was 1:0.29 (See Table 2 and Methods). This ordering is in agreement with the conversion rates of precursors having 14:1 at the sn2, i.e. conversion to 18:1 was preferred to 18:2 in a ratio of 1:0.71. Based on the integrative analysis described above, we determined that the deacylation rates of different chain types decrease in the order 14:0 > 14:1 > 22:6 > 18:3 (1:0.27 : 0.14 : 0.1). It is interesting to note that the saturated or monounsaturated chains are removed faster than polyunsaturated ones, thus providing a possible explanation why the sn2 position is enriched in polyunsaturated acyl chains. Removal of 18:1 from the sn2 position also appears to be slower than that of 14:0 and 14:1. An unexpected observation is that the sn2 22:6 chain of 18:0-22:6 PE precursor converts to 20:4 much faster than to 18:1. This conflicts with the reacylation rates predicted from the behavior of a 14:1 chain at sn2, which is replaced by 18:1 twice as fast as by 20:4 in the 14:1-14:1 precursor. This phenomenon is worth further investigation as it may indicate a cooperative interaction between sn1 and sn2 chain remodeling.

We also observed consistencies in secondary effect parameters. For instance, the sn1 16:1 to 18:1 conversion rate was found to be 0.0395 for the 14:0-14:0 precursor and 0.0358 for the 18:1-18:1.

Table 2. Remodeling rate parameters from six independent experiments.

| Experiment precursor | new sn1 chain | new sn2 chain |
|----------------------|---------------|---------------|
|                      | Initial chain |               |
|                      | 18:1 | 18:0 | 16:1 | 16:0 |           |
|----------------------|-------|------|------|------|-----------|
| 14:0-14:0            | 14:0  | 0.0889 | 0.0166 | 0.0261 | -         |
| 14:1-14:1            | 14:1  | 0.5903 | 0.1083 | -     | -         |
| 18:3-18:3            | 18:3  | 0.2500 | 0.0650 | 0.0589 | -         |
| 18:0-22:6            | 18:0  | 0.0673 | -     | -     | 22:6      | 0.0724 | -     |
| 18:0-18:1            | 18:0  | 0.0700 | -     | -     | 18:1      | -     | -     |
| 18:1-18:1            | 18:1  | -    | 0.0019 | 0.0072 | 0.0041 | 18:1 | -     | 0.0029 | -     |

Inferred remodeling rate parameters from six independent experiments. A "-" indicates unmodeled reactions either due to missing species or low flux in the experiment. The sn1 18:0 to 18:1 rate parameters inferred from two precursor experiments are similar: 0.0673 and 0.07 for the respective 18:0-18:1 and 18:0-22:6 experiments. The sn1 rate parameters of the first row have ratios 1:0.19:0.29, similar to ratios in the second row 1:0.18: - and third row 1:0.26:0.24. This indicates that the relative reacylation rates of 18:1, 18:0, and 16:1 are consistently ranked across experiments. Likewise, by comparing values within a column, we can determine relative deacylation rates, i.e. 14:1 > 18:3 > 14:0 at ratios 0.58:3:1 at the sn1 position. Analogous behavior was also observed for the sn2 position (See Supporting Information S1 for details).

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precursor. Also, the sn2 18:2 to 18:1 conversion rates were
determined to be 0.0388 for the 14:0-14:0 precursor and 0.0396
for the 18:1-18:1 precursor. Since these inferences are based on
conversions from lower abundance acyl species not originating in
any precursor, they may be more sensitive to experimental errors.
Future experiments with precursors having sn1 16:1 or sn2 18:2
would be beneficial to determine the accuracy of the approach for
secondary rate parameters.

Discussion

Due to the complexity of lipid remodeling and the lack of
previous computational tools, quantitative interpretations of
lipidomic data have been rare [1]. In this work, we have presented
the first method for inferring the processes and kinetic parameters
of phospholipid remodeling from lipidomic data. This method
required two steps: network structure inference using a fast
correlation analysis step, and inference of kinetic parameters
through an efficient B-Spline based optimization approach for
fitting the dynamical system. This work provides a significant
advance compared to previous lipidomic data mining approaches
for acyl chain remodeling, which focused on steady-state systems
[19] or were based on dynamic simulations without an explicit
method for parameter inference [20]. These acyl chain remodeling
studies are complementary to works addressing metabolic fluxes
between classes of lipids with different head groups [28,29].

By applying our new method, we have revealed a number of
important facts about lipid remodeling. We have shown that 18:1
is the predominant reacylated acyl chain at both sn1 and sn2
positions, consistent with previous findings [21]. We were also able
to determine the deacylation and reacylation rates of different
types of acyl chains. For example, we found that unsaturated
chains are cleaved off more rapidly than saturated ones at the sn1
position (14:1 > 18:3 > 14:0 > 18:0), while at the sn2 position
saturated chains are more quickly removed (14:0 > 14:1). These
data explain why saturated acyl chains are predominant in the sn1
position and unsaturated chains are predominant in the sn2
position of diacyl glycerophospholipids.

To appreciate the importance of the computational modeling
approach we have developed, it is useful to compare the results
with those that would have been deduced by empirical observation
of the data. Figure 6 shows the distribution of acyl chains at the
sn1 position of PE at the final time point in each experiment,
normalized by the amount of 18:1 at the sn1 position (See also
Supporting Information S1). This is when the experiments have
had the most time to equilibrate, so if similar remodeling processes
are occurring in each experiment we would expect the acyl
distributions to be similar. However, we observe that there are still
substantial residual effects from the precursors. The most salient
effects are that there are much larger amounts of 18:0 at the sn1
position in the 18:0-22:6 and 18:0-18:1 precursor experiments
than in the other precursor experiments. Under purely empirical
interpretation, this precursor bias might lead one to believe that
remodeling processes differ across experiments. However, our
quantitative modeling approach allowed us to determine that
remodeling processes are in fact consistent across experiments. It
is remarkable that our simulations not only all provide good fits but
also cross validate in the parameter values, despite the fact that
mass spectrometry measurements used to obtain the raw data have
some positional isomer and missing data uncertainties. This
suggests that the model is not excessively sensitive to measurement
uncertainties and thus captures the essential features of the
remodeling process in vivo.

Empirical interpretation also has other shortcomings. For
example, while the prior empirical interpretation suggested several
interactions between sn1 and sn2 chains [21], our modeling
approach indicates that the data can be well fit even if sn1 and sn2
chains react independently. Our modeling approach also has the
advantage of providing quantitative estimates of kinetic
parameters, which are non-obvious in empirical analysis. For example, we
were able to determine that the sn1 deacylation rate varies by an
order of magnitude depending on the type of acyl chain.

A strength of our method is that it is based on the straightforward position-independence assumption [26], which
has previously found to be valid in most contexts for the tetra-acyl phospholipid cardiolipin [19]. The success of the present model
indicates sn-position independence is typical for glycerophospholipid acyl chain remodeling. While certainly models involving
large number of parameters and more cooperative effects should
be able to fit the data, we have focused on an independence model
due to the standard criterion of wishing to keep the number of
parameters to a minimum. However, we do note that occasional
deviations from independence were observed in this study, e.g. in
the analysis of sn2 reacylation behaviors, suggesting that in a few
cases interactions among the acyl chains may influence the
remodeling process. This interaction/cooperativity could relate to
overall molecular hydrophobicity, which has been recently
strongly implicated in the specificity of A-type phospholipases [30].

In summary, we have constructed a powerful modeling tool for
the analysis of glycerophospholipid remodeling pathways and their
kinetics. The present work demonstrates that computational
methods can quantitatively determine the details of glycerophospholipid remodeling by identifying the specificity and kinetics of
deacylation and reacylation. Notably, the present method can be
readily extended to other glycerophospholipid classes and should
thus allow one to obtain a comprehensive picture of lipid
remodeling, which will be essential for understanding lipid
homeostasis in mammalian cells. A natural future application will
be determining the mechanistic impact of various types of
perturbations, e.g. knockdown of putative remodeling enzymes.
Software implementations for the Correlation Network (JAVA)
and Dynamic Simulation (MATLAB) are available at http://
nbidiaz.github.com/DLipid/.

Methods

Network Inference

The remodeling pathway of phospholipids can be thought of as
a directed weighted graph $G=(V,E)$ where the nodes represent
certain lipid species $s_i$, $1 \leq i \leq n$, and the directed edges $e_{ij}$,$1 \leq i,j \leq n$
indicates the flux. Here $n$ denotes the total number of species. The
weight of each edge is proportional to the degree of the flux from
source species to the target species. Here we describe a novel
algorithm for inferring such a network from MS time course
measurement such as in pulse chase experiments. Let $T = \{t_i\}_{i=1}^m$
be the measurement times, and $m$ is the total number of
measurements. At each time point $t_i$ all species whose concentra-
tion levels are decreasing in the next time point, at a significance
level $p_i$ as determined by t-test, are identified as possible
remodeling sources. By a source we mean a species that is
remodeled into a target species. The significance level $p_i$
depends on the time point and is defined by $p_i = \frac{\theta}{t_{i+1} - t_i}$. In practice,
parameter inferences are relatively insensitive to the choice of
significance level. An example of this is shown in Table 3.

Denote the set of candidate sources at the $i$th time point by $P_i$.
For each $z \in P_i$, we define the neighborhood $N(z)$, to be the set of
lipid species $\beta$ that share exactly one chain with $\alpha$. Next we introduce a correlation function that helps to determine whether $\beta \in N(\alpha)$ could be the remodeling product of $\alpha$. For a lipid species $\gamma$, define

$$sgn(\gamma) = sgn(\gamma_{i+1} - \gamma_i)$$

where the $sgn(\gamma_i)$ is determined according to the t-test at the significance level $p_i$. Let

$$cor(\alpha, \beta, t_i, t_m, p, \theta) = \delta(\alpha, \beta, t_i, t_m, p, \theta) \times$$

$$\sum_{h = t_i}^{t_m} |(\alpha_{h+1} - \alpha_h) (\beta_{h+1} - \beta_h)|$$

where $\delta(\alpha, \beta, t_i, t_m, p, \theta)$ is a sign function that is negative if $sgn(\alpha_h) \times sgn(\beta_h) < 0$ for all $i \leq h < m$ and positive otherwise. This $\delta$ function is introduced to capture the inverse relation between the concentrations of $\alpha$ and $\beta$ over the entire time interval $[t_i, t_m]$. Note that $[\alpha_h]$ and $[\beta_h]$ denote the concentration of $\alpha$ and $\beta$ species at $h$th time point, respectively.

For each candidate source $\alpha$, we associate a set $E(\alpha)$ of edges. The set $E(\alpha)$ is initialized to the empty set. We then cycle through candidate target set $N(\alpha)$, and for each member $\beta \in N(\alpha)$, we add an edge $e_{\alpha \beta}$ to $E(\alpha)$ if $cor(\alpha, \beta, t_i, t_m, p, \theta) < 0$ or if there exist a species $\gamma \in N(\beta)$ such that $cor(\alpha, \gamma, t_i, t_m, p, \theta) < 0$. The second correlation is introduced to account for the possibility that $\beta$ is remodeled to $\gamma$ which reduces the concentration of $\beta$. $\theta$ is defined as the significance threshold value in Algorithm 1 (Supporting Information S1). We select the $\gamma$ with highest correlation value. Since the concentrations of species vary in time, some fluxes may only be visible at later time intervals. These new fluxes may influence the correlations at the earlier time points. For this reason, If no negative correlation is found in the time interval $[t_i, t_m]$, the final time point $t_m$ is reduced to the previous time point $t_{m-1}$ and the whole process is repeated. We do this until an edge is found or we reach $t_{i+1}$. These recursions are repeated for the entire source set. Lastly, the weights of the edges are set to the correlation values. See SI for the pseudo-code of this algorithm.

### Table 3. The primary parameter values of 14:0-14:0 experiment are stable using different correlation network thresholds.

| threshold | num edges | num para | error | sn1 | sn2 | sn2 | sn2 |
|-----------|-----------|----------|-------|-----|-----|-----|-----|
|           | 14:0→18:1 | 14:0→16:1 | 14:0→18:0 | 14:0→18:2 | 14:0→18:1 | 14:0→18:2 |
| 0.1       | 16        | 14       | 400   | 0.0893 | 0.0312 | -   | 0.6197 | -   |
| 0.2       | 26        | 22       | 394   | 0.0911 | 0.0256 | 0.0213 | 0.5260 | 0.1216 |
| 0.3       | 32        | 24       | 387   | 0.0889 | 0.0261 | 0.0166 | 0.5176 | 0.1520 |
| 0.4       | 50        | 38       | 372   | 0.0801 | 0.0269 | 0.0130 | 0.3836 | 0.1062 |
| full      | 66        | 50       | 371   | 0.0688 | 0.0242 | 0.0163 | 0.3426 | 0.1018 |

Each row indicates the number of edges, number of parameters, fit error, and inferred parameter values at a given significance threshold for determining edges in the correlation network.

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Dynamic Simulations

The remodeling process of PE is a dynamical system that can be modeled by a set of coupled differential equations. This dynamical system depends on the rates of conversion of PE species into one another. These rates are not known a priori. Denote these parameters by the vector \( \mathbf{a} = (a_1, \ldots, a_N)^T \in \mathbb{R}^N \), where \( N \) denotes the total number of parameters. Let \( \mathbf{x} \in \mathbb{R}^N \) represent the vector of PE concentrations. Here \( N \) denotes the total number of species. The dynamical system describing the PE remodeling is then

\[
\frac{dx}{dt} = f(x, \mathbf{a})
\]  

(3)

Given a set of observations \((\mathbf{x}(t))_{i=1}^{n}\), there are a number of available numerical approximations that can be used to approximate the parameters \( \mathbf{a} \) using the observed time-course measurements, while simultaneously solving the differential equations [31–33]. Since the dependence of the vector field on the parameters is linear (See Table 1 for an example), we may rewrite the parameter inference problem as a minimization problem that can be efficiently solved using Singlular Value Decomposition, SVD, or QR decomposition as described in [27]. We write the solution \( \mathbf{u}(t) \) of the above system as a linear combination of cubic B-splines,

\[
\mathbf{u}(t) \approx \mathbf{x}(t)
\]  

(4)

\[
\mathbf{u}(t) = \sum_{j=0}^{p} \mathbf{b}_j \mathbf{B}_j(t)
\]  

(5)

where \( \mathbf{B}_j(t) \) are the B-splines and \( \mathbf{b}_j \in \mathbb{R}^N \) are the spline coefficients [34,35]. Define the error function \( E_D(\mathbf{b}) \) as the square of the distance of the solution \( \mathbf{u}(t) \) to the observation points as follows.

\[
E_D(\mathbf{b}, \mathbf{a}) = \sum_{i=1}^{n} \left\| \sum_{j=0}^{p} \mathbf{b}_j \mathbf{B}_j(t) - \mathbf{x}(t) \right\|^2
\]  

(6)

Our goal is to minimize the above error function, while simultaneously ensuring that the solution satisfies the differential equations. The constraint that \( \mathbf{u} \) has to satisfy the differential equations second constraint can also be stated in terms of a minimization problem. More precisely, if we have estimates \( \mathbf{u}(r_k) \) of the solution at the so-called “collocation points”, \( r_k \), we can define the error function

\[
E_M(\mathbf{b}, \mathbf{u}) = \sum_{k=1}^{n} \left\| \sum_{j=0}^{p} \mathbf{b}_j \frac{d \mathbf{B}_j(t)}{dt} - f(\mathbf{u}(r_k), \mathbf{a}) \right\|^2
\]  

(7)

which yields the overall error function

\[
E(\mathbf{b}, \mathbf{u}, \mathbf{a}) = \lambda E_D(\mathbf{b}, \mathbf{a}) + E_M(\mathbf{b}, \mathbf{u})
\]  

(8)

where \( \lambda \) is a weight parameter that controls the weight given to the observations versus the differential equations. Note that the since the dependence of \( f \) on \( \mathbf{a} \) is linear, \( E \) is linear in \( (\mathbf{b}, \mathbf{a}) \). This minimization problem is then readily solved using SVD or QR decomposition. In practice, the approximations \( \mathbf{u}^{(m)} \) are fitted in an iterative manner where at the \( m^{th} \) step, \( E \) is minimized with respect to \( (\mathbf{b}, \mathbf{a}) \) and the resulting \( \mathbf{b} \) is used to generate the new estimate \( \mathbf{u}^{(m+1)} \). The initial estimate \( \mathbf{u}^{(0)} \) is set to the solution of the minimization of Equation 6. In our calculations the \( \lambda \) parameter was set to 100. 5 B-splines were used for initial shooting, 21 B-splines and 49 \((l_{red} - l_{start} + 2 + 1)\) collocation points were used for precise approximation to the real function. We iterated for at least 1000 steps and then stopped at the solution which gives the minimum error among the last 6 steps, to correct for periodicity issues. The algorithm also stops when the error changes too slowly, i.e. \(<0.0001\) between two subsequent steps. Improvement of the fit from the initial guess was in general large and occurred rapidly in the first few steps of the iterative process (Supporting Information S1). Some parameters exhibited periodicity in the convergence process, which may be related to the shape of the solution space. In such situations, we only tracked the solution set which gives the lowest error. These other periodic solutions yielded parameter values which were similar to the solution with the lowest error (Supporting Information S1).

As an additional verification, the inferred parameters were used to independently solve the differential equation using standard numerical techniques. In our implementation we used the matlab function ode45 with stepsize 0.01 with initial conditions and remodeling rates as solved by the dynamic algorithm.

Deacylation and Reacylation Rates

Deacylation and reacylation rates were calculated from the \( k \) values given in Table 2. Note that in Table 2 the conversion rates 14:0–18:1 and 14:0–18:0 have a ratio of 5.36, which is relatively similar to the ratio of the rates 14:1–18:1 and 14:1–18:0 (4.55) and the ratio of 18:3–18:1 and 18:3–18:0 (3.85). This suggests that new acyl chains are added onto lysophospholipids by a similar process in all experiments. One possible explanation for this is that the pool of available acyl chains is similar in all experiments, which is reasonable since in all experiments of the same were used in the single experiments and because the acyl distribution becomes increasingly similar in all experiments over time [21]. Assuming that chain-specific reacylation processes are similar in different precursor experiments, absolute conversion rates therefore differ across experiments because of differences in chain-specific deacylation rates. Based on this logic, relative deacylation rates can be determined from the ratio of values between rows, while relative reacylation rates can be determined from the ratios of values between columns. For each comparison, deacylation and reacylation rate ratios were calculated via an average using the rates found to exist in the inferred network.

The relative ratios between rows and columns can be formally shown to indicate relative deacylation and reacylation rates by consideration of the kinetics of all species and deacylated intermediates using the steady state approximation for the intermediates. This approximation is justified by the fact that fully acylated PE is more prevalent than lyso- species in typical cells. Since the sn1 and sn2 positions are generally independent, we can consider the behavior of the sn1 (or sn2) position alone. For each chain type \( x_i \) at the sn1 position, the kinetics of \( x_i \) are given by \( d[x_i]/dt = -k^{(0)}[x_i] + k^{(0)}[I] \), where \( k^{(0)} \) is the deacylation rate of \( x_i \) and \( k^{(0)} \) is the reacylation rate of \( x_i \) and \( [I] \) is the concentration of the deacylated intermediate. Assuming that all deacylations lead to the intermediate \( I \) and that \( d[I]/dt = 0 \), solution of the set of linear equations yields that the rate parameter in Table 2 from initial chain \( i \) to new chain \( j \) is \( k^{(0)}k^{(0)}/\sum_i k^{(0)} \). From this it follows that the ratios of rows and columns indicate relative deacylation and reacylation rates. For example, for relative reacylation rates of chain types \( x \) and \( \beta \) we have \( (k^{(0)}k^{(0)}/\sum_i k^{(0)})/(k^{(0)}k^{(0)}/\sum_i k^{(0)}) = k^{(0)}/k^{(0)} \). For relative deacy-
Mass Spectrometry Data Analysis

The kinetics of remodeling were derived from data obtained by using neutral loss scanning which allows selective detection of labeled vs. unlabeled PE molecules, but does not provide definitive information on the acyl substituents or their sn-positions. However, such information was obtained in separate experiments in which the cellular PE molecules were fragmented using collisionally-activated decomposition and the products were analyzed as described in [21]. Several studies have shown that the identification of the acyl substituents and the assignment of their sn-positions in glycerophospholipids can be obtained by using such an approach [36–38]. Our own studies with several pairs of PE positional isomers yielded three main types of product ions: i) fatty acid carboxylate anions, ii) lysoPL formed upon neutral loss of PE positional isomers in the cellular PE species can be quantified with an error less than 10%.

Supporting Information

Supporting Information S1  Supporting information. (PDF)

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Author Contributions

Conceived and designed the experiments: LZ NDD KZ JC. Performed the experiments: LZ NDD KZ JC. Analyzed the data: LZ NDD KZ JC. Contributed reagents/materials/analysis tools: MH PS. Wrote the paper: LZ NDD KZ MH PS JC. Developed and implemented the dynamic algorithm: LZ. Developed and implemented the network algorithm: NDD. Conceived the idea of the dynamic and the network algorithms and developed the algorithms: KZ.

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