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| Citation       | Li, William Wei-Liang, Ronald A. Iltis, and Moe Z. Win. “Integrated IMU and Radiolocation-Based Navigation Using a Rao-Blackwellized Particle Filter.” 2013 IEEE International Conference on Acoustics, Speech and Signal Processing (May 2013). |
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| As Published   | http://dx.doi.org/10.1109/ICASSP.2013.6638647                                                                                                                                                                                                                 |
| Publisher      | Institute of Electrical and Electronics Engineers (IEEE)                                                                                                                                                                                                     |
| Version        | Author's final manuscript                                                                                                                                                                                                                                   |
| Accessed       | Tue Dec 18 01:10:01 EST 2018                                                                                                                                                                                                                               |
| Citable Link   | http://hdl.handle.net/1721.1/97201                                                                                                                                                                                                                         |
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Integrated IMU and Radiolocation-based Navigation Using A Rao-Blackwellized Particle Filter

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Abstract—In this paper, we develop a cooperative IMU/radiolocation-based navigation system, where each node tracks the location not only based on its own measurements, but also via collaboration with neighbor nodes. The key problem is to design a nonlinear filter to fuse IMU and radiolocation information. We apply the Rao-Blackwellization method by using a particle filter and parallel Kalman filters for the estimation of orientation and other states (i.e., position, velocity, etc.), respectively. The proposed method significantly outperforms the extended Kalman filter (EKF) in the set of simulations here.

Index Terms—Cooperative localization, navigation, inertial measurement unit (IMU), information fusion, particle filter.

I. INTRODUCTION

Navigation enables numerous emerging wireless applications in commercial, public and military operations [1]–[4]. Conventional techniques based on the global positioning system (GPS) often fail to provide reliable position information in harsh and indoor environments, due to the inability of GPS signals to penetrate many obstacles. For these reasons, GPS-less navigation using compact IMUs [5]–[8] and ultrawideband-based radiolocation [9]–[11] is of great current interest.

Inertial measurement units (IMU) have been widely adopted in assisting navigation when the GPS signal is severely attenuated and distorted. The IMU usually contains accelerometer and gyroscope sensors, measuring force and angular velocity, respectively. However, IMU-based navigation is accurate only for a short period of time due to the cubic error drift [12]. Recent work [12], [13] considered a foot-mounted IMU strategy which adopts step detection to correct the error. The drawback is that the step detection could introduce additional bias and drift, which degrades the navigation performance.

The accuracy of IMU-based navigation depends on the IMU model and filter design. In [14], a linear Gaussian drift model for IMU-derived position estimates is assumed by a Kalman filter. However, a more realistic IMU model is nonlinear due to coupling of orientation and acceleration measurements. The extended Kalman filter (EKF) is commonly used in such nonlinear applications and can generate divergent position/orientation estimates. Hence, the design of a more accurate, but computationally tractable nonlinear IMU filter remains a significant challenge.

In this paper, we develop a cooperative IMU-based navigation system, which fuses IMU measurement and radiolocation information to track the mobile node positions. The major contributions are summarized as follows:

• We design a Rao-Blackwellized particle filter (RB-PF) for IMU-based navigation. The proposed method significantly outperforms the EKF in the simulations here, and achieves much better convergence.

• We integrate the position information derived from IMU and radiolocation to achieve highly accurate navigation in both line-of-sight (LOS) and non-line-of-sight (NLOS) environments.

• We improve the navigation accuracy by using cooperative localization among the mobile nodes. The simulation results validate the importance of cooperation in navigation.

II. DYNAMIC AND MEASUREMENT MODEL FOR IMU

In this section, we describe the process model and the measurement model of the IMU. We define \( \varphi_k(n) \) as the IMU orientation with respect to the reference frame, and \( x_k(n) \) as a state vector containing position, velocity, acceleration, and the first-order derivative of orientation, given by

\[
x_k(n) = [x_k(n), y_k(n), \dot{x}_k(n), \dot{y}_k(n), \ddot{x}_k(n), \ddot{y}_k(n), \dot{\varphi}_k(n), \ddot{\varphi}_k(n)]^T.
\]

The IMU process model can be written as

\[
x_k(n + 1) = F x_k(n) + G w_k(n) \tag{1}
\]

\[
\varphi_k(n + 1) = \varphi_k(n) + T \dot{\varphi}_k(n) + \frac{T^2}{2} w_{k,\varphi}(n) \tag{2}
\]

where

\[
F = \begin{bmatrix}
I_2 & T I_2 & T^2/2 I_2 & 0 \\
0_2 & I_2 & T I_2 & : \\
0_2 & 0_2 & I_2 & 0 \\
0 & 0 & 0 & 1
\end{bmatrix},
G = \begin{bmatrix}
T^3/6 I_2 & 0 \\
T^2/2 I_2 & : \\
T I_2 & 0 \\
0 & 0 & T
\end{bmatrix}
\]

with the sample time \( T \), and \( I_n \) and \( 0_n \) denoting the \( n \times n \) unit matrix and zero matrix, respectively. The noise vector

\[w_k(n) = \begin{bmatrix}
G \nu_k(n) \\
0_2 \nu_k(n) \\
0_2 \nu_k(n) \\
0_2 \nu_k(n)
\end{bmatrix}
\]

\[w_{k,\varphi}(n) = \begin{bmatrix}
0_2 \nu_k(n) \\
0_2 \nu_k(n) \\
0_2 \nu_k(n) \\
0_2 \nu_k(n)
\end{bmatrix}
\]

The noise vector for such nonlinear applications and can generate divergent position/orientation estimates. Hence, the design of a more accurate, but computationally tractable nonlinear IMU filter remains a significant challenge.

We focus on the 2-D case, and the model can be extended to the 3-D case.

This research was supported, in part, by the National Science Foundation under Grant ECCS-0901034, the Office of Naval Research under Grant N00014-11-1-0397, the Defense University Research Instrumentation Program under Grant N00014-08-1-0826, and the MIT Institute for Soldier Nanotechnologies.
where (4) is an approximation of $p(\varphi_k^n(1)\mid \varphi_k^{i,n-1}, z_k^n)$ due to the computability issue, and $P_{\varphi_k,n}^0(n|n-1)$ in (5) is the covariance matrix of $\varphi_k^n(1)$.

Then the weight is derived as follows:

$$w_k^n(n) \triangleq \frac{p(\varphi_k^{i,n} | z_k^n)}{q(\varphi_k^{i,n} | z_k^n)} = p(z_k^n | \varphi_k^{i,n}) \frac{1}{p(z_k^n | \varphi_k^{i,n})} \frac{1}{q(\varphi_k^{i,n} | z_k^n)} = p(z_k^n | \varphi_k^{i,n}, z_k^{n-1}) \cdot w_k^{i,n}(n-1) \quad (6)$$

$$= w_k^n(n-1) \cdot N\left( z_k(n); H(\varphi_k^{i,n}(n))\hat{x}_k^n(n-1), H(\varphi_k^{i,n}(n))P_{\varphi_k,n}^0(n|n-1)H(\varphi_k^{i,n}(n))^T + R_k \right) \quad (7)$$

where the approximation $q(\varphi_k^{i,n-1} | z_k^n) \approx q(\varphi_k^{i,n} | z_k^{n-1})$ is made in (4) again for computability [20].

The particle filter contains a resampling procedure when the effective sample size [20] falls below a threshold [18], [21]. We choose the systematic resampling (Algorithm 2 in [20]) for simplicity of implementation.

**B. Kalman Filter for Estimating $\hat{x}_k^n(1)$**

The non-orientation states including position, velocity, and derivative, can be modeled as linear Gaussian, once the orientation is estimated. Hence, the Kalman filter is optimal for estimating $\hat{x}_k(n)$ given the particle stream $\varphi_k^{i,n}$. Specifically, we use $N_s$ parallel Kalman filters to estimate $\hat{x}_k^n(i)$, $i = 1, \cdots, N_s$. The Kalman filter gain is derived as

$$K_k^i(n) = P_k^i(n|n-1)H^T(\varphi_k^n(i)) \left( H(\varphi_k^n(i))P_k^i(n|n-1)H^T(\varphi_k^n(i)) + R_k \right)^{-1}. \quad (8)$$

The correction steps are given by

$$\hat{x}_k^n(i,n) = \hat{x}_k^n(i,n-1) + K_k^i(n) \left( z_k(n) - H(\varphi_k^n(i))\hat{x}_k^n(i,n-1) \right) \quad (9)$$

$$P_k^i(n|n) = \left( I - K_k^i(n)H(\varphi_k^n(i)) \right) P_k^i(n|n-1). \quad (10)$$

The prediction steps are given by

$$\hat{x}_k^n(i,n+1) = F \hat{x}_k^n(i,n) \quad (11)$$

$$P_k^i(n+1|n) = FP_k^i(n|n)F^T + GQ_kG^T. \quad (12)$$

The overall RB-PF for IMU-based navigation is described in Algorithm 1.

**IV. INTEGRATED IMU/RADIOLOCATION NAVIGATION**

In this section, we develop a cooperative navigation algorithm, which fuses the RB-PFs for IMU measurements and the Kalman filter for cooperative radiolocation.

\footnote{It is difficult to directly compute $p(\varphi_k^{i,n} | \varphi_k^{i,n-1}, z_k^n)$, since both $\varphi_k^n(i)$ and $P_{\varphi_k,n}^0(n|n)$ depend on $\varphi_k^n(1)$, which is not available.}
Algorithm 1: Rao-Blackwellization Algorithm for the IMU-based Navigation

Require: $\varphi_k^i(n-1)$, $\hat{x}_k^i(n|n-1)$, $P_k^i(n|n-1)$ and the measurement $z_k(n)$

1: for $i = 1, \ldots, N_k$ do
2: Generate particle $\varphi_k^i(n) \sim N(\varphi_k^i(n-1) + T \hat{\varphi}_k^i(n-1), T^2 P_k^i(n|n-1) + T^2 \sigma_n^2)$
3: Update the weight $w_k^i(n)$ via (7)
4: Update $\hat{x}_k^i(n|n)$ and $P_k^i(n+1|n)$ via (8)–(10)
5: Predict $\hat{x}_k^i(n+1|n)$ and $P_k^i(n+1|n)$ via (11)–(12)
6: end for
7: Normalize the weights by $\tilde{w}_k^i(n) = w_k^i(n) / \sum_{i=1}^{N_k} w_k^i(n)$, $\forall i = 1, \ldots, N_k$
8: Calculate effective sample size $\tilde{N}_{\text{eff}} = 1 / \sum_{i=1}^{N_k} (\tilde{w}_k^i(n))^2$
9: if $\tilde{N}_{\text{eff}} \leq N_T$ then
10: Systematical resampling (cf. [20]) of $\varphi_k(n)$, and $w_k^i(n) = 1/N_k$
11: end if
12: Calculate the estimated states: $\hat{\varphi}_k(n) = \sum_{i=1}^{N_k} w_k^i(n) \varphi_k^i(n)$ and $\hat{x}_k(n|n) = \sum_{i=1}^{N_k} w_k^i(n) \hat{x}_k^i(n|n)$.

V. SIMULATION RESULTS

In this section, we simulate the cooperative IMU-based navigation algorithm in an urban corridor scenario.

The urban corridor is illustrated in Fig. 2, where the street is 15 m wide with buildings 15 m wide on the north and south sides. Five anchor nodes are placed on the west end of the street, and five mobile nodes move at a nominal velocity of 1 m/s heading east, and gradually spread out into the buildings on two sides. The mobile nodes are also rotating themselves, with the small bar on each node denoting the orientation. The movements and rotations are generated according to the Gaussian IMU process model in (1)–(2). Range measurements $z_{k,j}$ are assumed to be LOS when both nodes $k, j$ are in the street, otherwise the measurements are modeled as NLOS. The LOS and NLOS range measurement RMS errors are based on [22] (Fig. 9). The anchor-to-mobile radio range is 100 m. The simulation parameters used are summarized in Table I.

For comparison, we also plot the average estimation error of an EKF, which uses a single nonlinear filter to estimate all the states. It shows that the RB-PF significantly outperforms the EKF, e.g., it reduces position error more than 50% as the nodes move towards the east. This is due to the loss of communications when nodes are beyond their radio range to anchors or other mobile nodes, or due to the NLOS conditions when nodes move into buildings.

TABLE I: Urban corridor simulation parameters

| Parameter                      | Value |
|--------------------------------|-------|
| Sample time: $T$               | 1 sec |
| Total simulation duration      | 600 sec |
| Number of simulation runs for error averaging | 16 |
| Number of particles: $N_k$    | 50 |
| Jerk noise standard deviation (STD): $\sigma$ | 5e-5 m/s^3 |
| Angular acceleration noise STD: $\sigma_\dot{\phi}$ | 5e-4 rad/s^2 |
| IMU gyro (angular velocity) noise STD: $\sigma_\phi$ | 8.7e-4 rad/s |
| IMU accelerometer (force) noise STD: $\sigma_f$ | 2e-3 m/s^2 |
| LOS range measurement RMS error: $\sigma_{\text{LOS}}$ | 9 m |
| NLOS range measurement RMS error: $\sigma_{\text{NLOS}}$ | 100 |
| Number of IMU updates per SDRS update: $N_{\text{SDRS}}$ | 0.1 sec |

Fig. 2: The urban corridor with mobile nodes trajectories.
Rao-Blackwellization uses multiple particles to estimate the angle, which results in better convergence compared with a single EKF.

In Fig. 4, we investigate the performance with different extents of node cooperation. Once the mobile nodes move beyond the anchor radio range, the radiolocation relies on inter-mobile range measurements and the IMUs. We consider two settings of mobile-to-mobile radio range: 30 m which results in partial cooperation beyond the middle of the corridor, and 45 m which generally yields full cooperation. We first simulate the urban corridor with buildings (Fig. 2) where both LOS and NLOS conditions exist. In Fig. 4a the 30 m and 45 m range shows that the estimation errors are similar, and the position error with the larger 45 m range is only slightly reduced by 2 m at the end. In Fig. 4b, we removed the two buildings so that LOS signals are always available. The result is a more significant improvement using the 45 m range/full cooperation, i.e., the position error is reduced by 5 m close to the end of the corridor. Hence, the simulation results here support the hypothesis that cooperation among mobile nodes improves the navigation accuracy, especially in the LOS environment.

VI. CONCLUSION

In this paper, we proposed a cooperative IMU-based navigation algorithm using RB-PFs. The IMU measurements and radiolocation information are integrated to improve the navigation accuracy. An urban corridor simulation shows that RB-PFs reduce the position error up to ten meters compared with EKF. Moreover, a significant improvement in angle estimation by a factor of six is observed using the proposed method. The results also demonstrate the importance of node cooperation in navigation, especially in the LOS environment.

This paper has focused on non-GPS navigation, which fuses IMU and radiolocation information. Previous work on IMU-based navigation, e.g., [12], [13], employ a foot-mounted IMU strategy and require step detection to correct the error, which could introduce additional bias and drift. Moreover, most prior research [5], [13]–[16] was limited to Kalman filter or EKF for navigation, which are not as well suited as PFs for the nonlinear IMU model. In this paper, we designed RB-PFs for IMU-based navigation, integrating the radiolocation information, which yields significant improvement on the navigation accuracy.
REFERENCES

[1] M. Z. Win, A. Conti, S. Mazuelas, Y. Shen, W. M. Gifford, D. Dardari, and M. Chiani, “Network localization and navigation via cooperation,” IEEE Commun. Mag., vol. 49, no. 5, pp. 56–62, May 2011.
[2] K. Pahlavan, X. Li, and J.-P. Mäkelä, “Indoor geolocation science and technology,” IEEE Commun. Mag., vol. 40, no. 2, pp. 112–118, Feb. 2002.
[3] H. Liu, H. Darabi, P. Banerjee, and J. Liu, “Survey of wireless indoor positioning techniques and systems,” IEEE Trans. Syst., Man, Cybern. C, vol. 37, no. 6, pp. 1067–1086, Nov. 2007.
[4] Y. Shen, S. Mazuelas, and M. Z. Win, “Network navigation: Theory and interpretation,” IEEE J. Sel. Areas Commun., vol. 30, no. 9, pp. 1823–1834, Oct. 2012.
[5] D. H. Titterton and J. L. Weston, Strapdown Inertial Navigation Technology. The American Institute of Aeronautics and Astronautics and The Institution of Engineering, 2004.
[6] I. Constandache, R. R. Choudhury, and I. Rhee, “Towards mobile phone localization without war-driving,” in Proc. IEEE Conf. on Computer Commun., San Diego, CA, Mar. 2010, pp. 1–9.
[7] C. Ascher, C. Kessler, M. Wankerl, and G. F. Trommer, “Dual IMU indoor navigation with particle filter based map-matching on a smartphone,” in Proc. Int. Conf. on Indoor Positioning and Indoor Navigation, Zurich, Switzerland, Sep. 2010, pp. 1–5.
[8] J. Han, E. Owusu, L. T. Nguyen, A. Perrig, and J. Zhang, “ACComplice: Location inference using accelerometers on smartphones,” in Proc. Int. Conf. on Commun. Syst. and Netw., Bangalore, India, Jan. 2012, pp. 1–9.
[9] S. Gezici, Z. Tian, G. B. Giannakis, H. Kobayashi, A. F. Molisch, H. V. Poor, and Z. Sahinoglu, “Localization via ultra-wideband radios: a look at positioning aspects for future sensor networks,” IEEE Signal Process. Mag., vol. 22, no. 4, pp. 70–84, Jul. 2005.
[10] Y. Shen, H. Wyneersch, and M. Z. Win, “Fundamental limits of wideband localization – Part II: Cooperative networks,” IEEE Trans. Inf. Theory, vol. 56, no. 10, pp. 4981–5000, Oct. 2010.
[11] K. Yu and I. Oppermann, “Performance of UWB position estimation based on time-of-arrival measurements,” in Proc. Int. Workshop on Ultra Wideband Syst., Oulu, Finland, May 2004, pp. 400–404.
[12] E. Foxlin, “Pedestrian tracking with shoe-mounted inertial sensors,” IEEE Comput. Graph. Appl., vol. 25, no. 6, pp. 38–46, Nov.-Dec. 2005.
[13] A. R. Jiménez, F. Seco, J. C. Prieto, and J. Guevara, “Accurate pedestrian indoor navigation by tightly coupling foot-mounted IMU and RFID measurements,” IEEE Trans. Instrum. Meas., vol. 61, no. 1, pp. 178 – 189, Jan. 2012.
[14] R. A. Itilis, “System-level algorithm design for radionavigation using UWB waveforms,” in Proc. Int. Telemetering Conf., San Diego, CA, Oct. 2012, pp. 1–10.
[15] I. Skog, “A low-cost GPS aided inertial navigation system for vehicular applications,” Master’s thesis, Royal Institute of Technology, Stockholm, Sweden, Mar. 2005.
[16] A. R. Jiménez, F. Seco, J. C. Prieto, and J. Guevara, “Indoor pedestrian navigation using an INS/EKF framework for yaw drift reduction and a foot-mounted IMU,” in Workshop on Positioning, Navigation and Commun. (WPNC), Dresden, Germany, Mar. 2010, pp. 135 – 143.
[17] F. Gustafsson, F. Gunnarsson, N. Bergman, U. Forssell, J. Jansson, R. Karlsson, and P. J. Nordlund, “Particle filters for positioning, navigation and tracking,” IEEE Trans. Signal Process., vol. 50, no. 2, pp. 425–437, Feb. 2002.
[18] B. Ristic, M. S. Arulampalam, and N. Gordon, Beyond the Kalman Filter: Particle Filters for Tracking Applications. Norwood, MA: Artech House, 2004.
[19] K. J. Kim, M.-O. Pun, and R. A. Itilis, “Joint carrier frequency offset and channel estimation for uplink MIMO-OFDMA systems using parallel Schmidt Rao-Blackwellized particle filters,” IEEE Trans. Commun., vol. 58, no. 9, pp. 2697 – 2708, Sep. 2010.
[20] M. S. Arulampalam, S. Maskell, N. Gordon, and T. Clapp, “A tutorial on particle filters for online nonlinear/non-Gaussian Bayesian tracking,” IEEE Trans. Signal Process., vol. 50, no. 2, pp. 174–188, Feb. 2002.
[21] Z. Chen, “Bayesian filtering: From Kalman filters to particle filters, and beyond,” McMaster University, Tech. Rep., 2003.
[22] D. Dardari, C.-C. Chong, and M. Z. Win, “Threshold-based time-of-arrival estimators in UWB dense multipath channels,” IEEE Trans. Commun., vol. 56, no. 8, pp. 1366–1378, Aug. 2008.