Tunable Spin dependent beam shift by simultaneously tailoring geometric and dynamical phases of light in inhomogeneous anisotropic medium

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Spin orbit interaction and the resulting Spin Hall effect of light are under recent intensive investigations because of their fundamental nature and potential applications. Here, we report an interesting manifestation of spin Hall effect of light and demonstrate its tunability in an inhomogeneous anisotropic medium exhibiting spatially varying retardance level. In our system, the beam shift occurs only for one circular polarization mode keeping the other orthogonal mode unaffected, which is shown to arise due to the combined spatial gradients of the geometric phase and the dynamical phase of light. The constituent two orthogonal circular polarization modes of an input linearly polarized light evolve in different trajectories, eventually manifesting as a large and tunable spin separation. The spin dependent beam shift and the demonstrated principle of simultaneously tailoring space-varying geometric and dynamical phase of light for achieving its tunability (of both magnitude and direction), may provide an attractive route towards development of spin-optical devices.

Spin orbit interaction (SOI) dealing with the coupling of spin and orbital degrees of freedom of massive (e.g., electron) and mass-less (e.g., photon) particles has led to several fundamental consequences in diverse fields of physics, ranging from atomic, condensed matter to optical systems. Since light can carry both spin (SAM, circular/elliptical polarization) and orbital angular momentum (OAM), on conceptual grounds, coupling and inter-conversion between the spin and orbital AM degrees of freedom of light is expected under certain circumstances. This leads to the SOI of light, and accordingly the evolution of polarized light in a trajectory mimics the SOI effect of a mass-less spin 1 particle (photon)1–4.

The SOI of light is typically manifested as two interdependent effects. The first one is the effect of the trajectory on the state of polarization of light, leading to the generation of spin (circular polarization)-dependent optical vortices, which usually takes place in cylindrically or spherically symmetric systems. The second one is the reverse effect of polarization on the trajectory of light, manifesting as a spin dependent shift of the trajectory of the light beam, known as the Spin Hall effect (SHE) of light1–5. This is usually associated with the breaking of the symmetry. The photonic SHE has been observed recently in various optical interactions1–5, each of which are discernable by important fundamental or applicative aspects. These are under recent intensive investigations because of their fundamental nature and also due to the fact that these are offering new opportunities for the development of spin-controlled photonic devices1,2,6,7. Note that generation of geometric phases (and its gradient) and subsequent conservation of the total angular momentum of light is intimately associated with the optical SOI phenomena. There are two variants of the geometric phase that contribute to the SOI phenomena—the spin redirection Berry phase and the Pancharatnam-Berry (PB) geometric phase. SOI effects produced via spin redirection Berry phase (e.g., in tight focusing of fundamental or higher order Gaussian beams, scattering from micro/nano systems, reflection/refraction at dielectric interfaces etc.), is generally weak1–4. Despite the fact that such tiny SHE

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A space varying Pancharatnam-Berry (PB) geometric phase \( \Phi_g(\xi) \approx \Omega_\xi \xi / \Omega_\xi ; \xi / \xi / \) manifests as input circular polarization (SAM) dependent shift in the transverse momentum distribution \( \Delta k_x \) of the beam. If one further introduces a spatial gradient of dynamical phase \( \Phi_d(\xi) \approx \Omega_\xi \xi / \Omega_\xi \), it may happen that for one circular polarization mode, the two spatial gradients cancel out to yield no net shift. For the other orthogonal mode, on the other hand, they may yield an accumulated shift of the beam centroid.

For a paraxial Gaussian beam, we neglect small longitudinal field component and represent the transverse components as

\[
|E_\perp(x, y)| = |\mathbf{e}| F(x, y)
\]

where \(|\mathbf{e}| = [\alpha_x, \alpha_y]^T\) is the Jones vector of the homogeneously polarized input beam and \(F(x, y)\) is its Gaussian envelop. On propagation through the inhomogeneous anisotropic medium, it acquires space varying dynamical \(\Phi_d(\xi)\) and PB geometric phase \(\Phi_g(\xi)\). The output field can be written as

\[
|E_\perp| = e^{i\phi_{\text{PB}}(\xi)} J_{2\xi}(\xi)|E_\perp|
\]

here, \(J_{2\xi}(\xi)\) is a \(2 \times 2\) matrix representing the effect of the PB geometric phase \(\Phi_g(\xi)\).

For input RCP \(|\mathbf{e}_R| = \frac{1}{\sqrt{2}}[1, i]^T\) and LCP \(|\mathbf{e}_L| = \frac{1}{\sqrt{2}}[1, -i]^T\) states, the output field becomes

\[
|E_\perp| = e^{i\Phi_g(\xi)} |\mathbf{e}_\xi| |E_\perp|
\]

here, \(\pm\) correspond to input RCP and LCP states, respectively.

The expectation values of the transverse co-ordinates and the momenta of the output beam can then be calculated as

\[
\langle \xi \rangle = \frac{\langle E_\perp \rangle}{\langle E_\perp \rangle}, \quad \langle k_{\perp x/y} \rangle = \frac{\partial_{\perp x/y} \langle E_\perp \rangle}{\langle E_\perp \rangle}
\]

For input RCP and LCP states, the quantities \(\xi = x/y\) and \(k_{\perp x/y}\) can be determined by using eq. (3) in eq. (4). While, \(\xi = x/y\) vanishes, yielding no net co-ordinate shift, the momentum shift becomes non-zero and determined by \(\Phi_g(\xi)\) and \(\Phi_d(\xi)\). When the two phases have equal gradient \(\partial_{\perp x/y} \Phi_g(\xi) = \partial_{\perp x/y} \Phi_d(\xi) = \Omega_\xi\), the momentum domain shifts for input RCP and LCP states become

\[
\langle k_{\perp x/y} \rangle_{\text{RCP}} = 2\Omega_\xi \quad \text{and} \quad \langle k_{\perp x/y} \rangle_{\text{LCP}} = 0
\]

We shall subsequently demonstrate that equal spatial gradients of geometric and dynamical phases can indeed be produced in a twisted nematic liquid crystal-based SLM by modulating its pixels with user controlled grey level distributions \((n)\). We now turn to the modeling of the evolution of PB geometric phase and dynamical phase of light in such system.

Pancharatnam-Berry (PB) geometric phase and dynamical phase in twisted nematic liquid crystal layers. When polarized light propagates through an anisotropic (birefringent) medium, it acquires
both PB geometric phase and dynamical phase. The dynamical phase for a linear birefringent medium is determined by the extraordinary and ordinary refractive indices \((n_e, n_o)\) and consequently it also depends upon the magnitude of linear retardance \(\delta\) (defined as \(\delta = \frac{2\pi}{\lambda} (n_e - n_o) d\), where \(d\) is the path length and \(\lambda\) is the wavelength). The PB geometric phase in such birefringent medium, on the other hand, is determined by the orientation angle of the anisotropy axis \(\theta\). Thus, in principle, one can produce equal spatial gradients of the dynamical phase and PB geometric phase in an inhomogeneous birefringent medium by controllably (and simultaneously) changing the magnitude of linear retardance \(\delta\) and the orientation angle of the anisotropy axis in the transverse plane \((x/y\)–plane, with \(z\) being the propagation direction of light). In case of a twisted nematic liquid crystal-based spatial light modulator (SLM), the system is slightly more complex. The SLM comprises of many layers of liquid crystals exhibiting linear birefringence with the axis of anisotropy of each layers twisted by an angle. The net anisotropy effects of such twisted birefringent layers manifest as both linear retardance and optical rotation. This optical rotation effect has geometric origin. In such system, while the total dynamical phase is primarily determined by the total accumulated linear retardance, the PB geometric phase is determined by the effective optical rotation. Since, the magnitudes of the linear retardance and optical rotation can be controlled by changing the grey level values \((n)\) in the SLM, one can controllably generate both geometric and dynamical phases of light, as described below.

The evolution of both the phase and the polarization of light in twisted nematic liquid crystal layers can be modeled using the following equation \(^{17}\)

\[
|e_o\rangle = e^{i\left(\frac{2\pi n_d}{\lambda} + \frac{\delta_{tot}}{2}\right)}R(-\psi)\left(A - iB\right)C|e_i\rangle = e^{i\left(\frac{2\pi n_d}{\lambda} + \frac{\delta_{tot}}{2}\right)}J(\psi, \delta_{tot})|e_i\rangle
\]

where, \(A = \cos\left(\frac{\psi^2 + \left(\frac{\delta_{tot}}{2}\right)^2}{\psi^2 + \left(\frac{\delta_{tot}}{2}\right)^2}\right)\); \(B = \frac{\delta_{tot}}{2} \sin\left(\frac{\psi^2 + \left(\frac{\delta_{tot}}{2}\right)^2}{\psi^2 + \left(\frac{\delta_{tot}}{2}\right)^2}\right)\);

\[
C = \psi^2 + \left(\frac{\delta_{tot}}{2}\right)^2
\]

Here, \(\delta_{tot} = \frac{\delta}{n} (n_e - n_o) d\) is the total linear retardance, \(n_e, n_o\) are the extraordinary and ordinary refractive indices, \(\psi\) is the twist angle, \(J\) is the Jones matrix of the system containing the \(2 \times 2\) rotation matrix \(R(-\psi)\). The evolution of polarization in SLM can also be alternatively modeled using the effective Jones matrix \((J_{eff})\) as a sequential product of matrices of an equivalent linear retarder \((J_{ret})\) with effective linear retardance \(\delta_{eff}\) and its orientation angle \(\theta_{eff}\) and an effective optical rotator \((\psi_{eff})\) \(^{18}\)

\[
J_{eff} = R(\psi_{eff})J_{ret}(\delta_{eff}, \theta_{eff})
\]

with \(\psi_{eff} = -\psi + 2\theta_{eff}\)

The dynamical phase (for input LCP/RCP states) is clearly given by the phase factor in eq. (6)

\[
\Phi_d(n) = \frac{2\pi}{\lambda} \left\{ \frac{n_e(n) + n_o}{2} \right\} d = \frac{\delta_{tot}(n)}{2} + \frac{2\pi}{\lambda} n_d d
\]

Here, \(n\) is the value of grey level(s) applied to a twisted nematic liquid crystal-based SLM (which is used to observe the spin specific beam shift in our experiments, as described subsequently). Henceforth, we only consider the first term in eq. (8), since, the grey level dependent part is only relevant to the effect. The matrix \(J\) (in eq. (6)) is free from dynamical phase \(\Phi_d = \arg \left\{ \frac{det(J)}{2} \right\} = 0\) \(^8\) and the corresponding PB geometric phase encoded in it, can be determined using the Pancharatnam connection \(^{19-21}\), for input RCP \((|e_R\rangle\) and LCP \((|e_L\rangle\) states as

\[
\Phi_{PB} = \arg \left\{ e_R \langle e_R| \right\} = +\psi_{eff}(n) \quad \text{and} \quad \Phi_{PB} = \arg \left\{ e_L \langle e_L| \right\} = -\psi_{eff}(n)
\]

As apparent from the above theoretical treatment, when polarized light propagates through twisted nematic liquid crystal layers, it acquires both dynamical and PB geometrical phases. The PB geometric phase arises here due to the non-cyclic polarization evolution \(^{19,21}\) in the twisted birefringent structure (due to the twist along the longitudinal direction). As shown in Eq. 9, the resulting PB geometric phase is determined by the effective optical rotation \(\psi_{eff}\) parameter, which has geometrical origin. The total dynamical phase, on the other hand, is determined by the total linear retardance \(\delta_{tot}\) parameter (see Eq. 8). Importantly, since both the \(\psi_{eff}\) and \(\delta_{tot}\) parameters can be controlled by changing the grey level values \((n)\) in the SLM, both the dynamical and the PB geometric phases can be simultaneously generated in a controlled manner. One can thus produce spatial gradients of the dynamical and the PB geometric phases by creating grey level gradient in the SLM along one chosen linear direction \((x\ or\ y)\) (see Methods). However, for this purpose, one needs to first experimentally determine the dependence of the \(\psi_{eff}(n)\) and \(\delta_{tot}(n)\) parameters on the grey level value \(n\). For producing equal spatial gradients of the two phases, one then needs to choose the range of grey levels for which the gradients \(\frac{d\psi_{eff}}{dn}\) and \(\frac{d\delta_{tot}(n)}{dn}\) are nearly equal.
Note that eqs (7, 8 and 9) in combination with experimental Mueller matrix measurements, can be used to determine both the geometric and the dynamical phases of light. For this purpose, full $4 \times 4$ Mueller matrices $M$ can be recorded from the SLM having uniform grey level ($n$) addressing. The effective linear retardance $\delta_{\text{eff}}(n)$ and optical rotation $\psi_{\text{eff}}(n)$ parameters can be determined from the elements of $M$, by representing it as a product of basis matrices of an equivalent linear retarder and rotator (Jones $\rightarrow$ Mueller matrix conversion of eq. 7) (see Supplementary Information). The twist angle of the SLM ($\psi$) can also be determined separately. Using these set of parameters, one can determine the magnitudes of total retardance $\delta_{\text{tot}}(n)$ from the relationship connecting them (derived from the equivalence of eqs 6 and 7).

$$
\delta_{\text{tot}}(n) = 2 \left\{ \cos^{-1} \left[ \cos \left( \frac{\delta_{\text{eff}}(n)}{2} \right) \cos(\psi_{\text{eff}}(n) + \psi) \right] \right\}^2 - \psi^2
$$

(10)

Thus obtained $\delta_{\text{tot}}(n)$ and $\psi_{\text{eff}}(n)$ parameters may finally be used to determine the values of $\Phi_{\text{d}}(n)$, $\Phi_{\pm}^\pm(n)$, and the resulting total phase $[\Phi_{\text{tot}}^\pm(n) = \Phi_{\text{d}}(n) + \Phi_{\pm}^\pm(n)$, $\pm$ corresponding to input RCP and LCP states, respectively].

In what follows, (i) we experimentally demonstrate the spin dependent beam shift and its tunability in an inhomogeneous anisotropic medium; (ii) We then determine both the space varying dynamical and the geometric phases in such system to demonstrate the underlying principle; (iii) Finally, we show large spin dependent splitting of input linearly polarized beam.

**Results and Discussion**

**Tunable Spin Specific Beam Shift in inhomogeneous anisotropic medium.** The inhomogeneous anisotropic medium was realized by modulating the pixels of a twisted nematic liquid crystal-based SLM by user controlled grey level ($n$) distributions (see Methods). Making use of the experimental arrangement (Fig. 1) and using varying spatial gradient of the grey levels in the SLM, spin dependent beam shift (shift in transverse momentum distribution $\pi k_2^-/y$) and its tunability is demonstrated in Fig. 2. The momentum domain beam shift for the input RCP state increases systematically with increasing spatial gradient of grey level ($\frac{dn}{dx} = x/\mu$). Remarkably, the shift of the beam centroid (momentum shift manifested as a shift of the centroid) becomes as large as ~25.16 $\mu$m for the highest applied spatial gradient $\frac{dn}{dx} = 0.0653$ bit/$\mu$m (varied between 11.56–25.16 $\mu$m for $\frac{dn}{dx} = 0.0205–0.0653$ bit/$\mu$m). The beam centroid for input LCP state, on the other hand, does not exhibit any appreciable shift (Fig. 2). While, these results are for applied grey level gradient along the x-direction, similar results were also obtained for that applied along the y-direction. We now proceed to determine the space varying
PB geometric phase and dynamical phase and relate these to the observed effect (the values of the spatial gradients of total phase \( \Phi_{\text{tot}}^{\pm}(n) \) for the RCP state noted in Fig. 2, are based on these, as described below).

**Determination of PB geometric phase and dynamical phase.** The geometric and the dynamical phases of light were determined from experimental Mueller matrix measurements in combination with the treatment outlined previously. Mueller matrices were recorded from the SLM having different uniform grey level \( n \) addressing (see Methods and Supplementary Information). The twist angle of the SLM was separately determined to be \( \psi = \pi/2 \). The results of the Mueller matrix measurements, determination of the medium polarization parameters \( \delta_{\text{eff}}(n), \psi_{\text{eff}}(n) \) and \( \delta_{\text{tot}}(n) \), and the corresponding dynamical \( \Phi_{\text{d}}(n) \) and geometrical phases \( \Phi_{\text{g}}^{\pm}(n) \) of light are summarized in Fig. 3. A typical Mueller matrix M recorded from the SLM for \( n = 120 \) is shown in

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**Figure 2. Experimental observation of tunable spin specific beam shift.** Transverse momentum distribution \( (\frac{\Delta k}{2\pi}) \mu m^{-1} \) of the transmitted beam for input LCP (middle panel) and RCP (bottom panel) states, for three representative spatial gradients of grey levels \( \frac{dn}{dx} = 0.0205, 0.0451, 0.0653 \text{ bit/\mu m} \) (right to left). Grey levels (values \( n = 30–170 \)) are shown using color bar and the spatial dimensions over which these were applied, are noted. Result for a uniform grey level distribution is displayed as reference (top panel). While, the beam centroid for input RCP state exhibits large and systematic shift with increasing \( \frac{dn}{dx} \), that for LCP state does not exhibit any appreciable shift, demonstrating spin specific beam shift and its tunability. The grey level dependence of total phase experienced by RCP state \( \Phi_{\text{tot}}^{+}(n) \) (shown using color bar) and the noted phase gradients are based on determination of geometric and dynamical phases, results of which are presented subsequently.
Fig. 3a, the elements are represented in normalized unit (normalized by the M11 element). The normalized values of the elements (between $-1$ to $+1$) are shown using the color bar. The Mueller matrices show characteristic features of pure retarders (Fig. 3a, and Supplementary Information). Specifically, the signatures of the effective linear retardance ($\delta_{\text{eff}}(n)$) is manifested in considerable magnitudes of the $M_{24}/M_{42}$ and $M_{34}/M_{43}$ elements. The corresponding signature of effective optical rotation ($\psi_{\text{eff}}(n)$) is reflected as a difference in the magnitudes of the $M_{23}$ and $M_{32}$ elements. The weak magnitudes and negligible variation of the elements of the 1st row and the 1st column of the matrices ($M_{12}/M_{21}$, $M_{13}/M_{31}$, $M_{14}/M_{41}$ elements, which encode polarization diattenuation effect$^{22,23}$) with varying $n$ implies negligible polarization dependent intensity modulation effect. The $\delta_{\text{eff}}(n)$ and the $\psi_{\text{eff}}(n)$ parameters were subsequently determined from the recorded Mueller matrices (see Supplementary Information).

The total linear retardance parameter $\delta_{\text{tot}}(n)$ was then determined using the values for $\delta_{\text{eff}}(n)$ and the $\psi_{\text{eff}}(n)$ in Eq. (10). From the estimated medium polarization parameters ($\delta_{\text{eff}}(n)$, $\psi_{\text{eff}}(n)$ and $\delta_{\text{tot}}(n)$ in Fig. 3b) it appears that for the range of grey levels ($n=30–170$) the $\psi_{\text{eff}}$ and the $\delta_{\text{tot}}$ parameters have nearly same gradient $d[\psi_{\text{eff}}(n)]/dn$ constant. The resulting total phase ($\Phi_{\text{tot}} = \Phi_{\text{tot}} + \Phi_{\text{tot}}^\prime$) derived using eqs 8, 9 and 10 and Fig. 3c) underscores the key feature pertinent to the observed spin dependent beam shift. The small (but non-zero) total phase gradient for input LCP state implies that $d[\psi_{\text{eff}}(n)]/dn$ is nearly but not exactly equal to $d[\psi_{\text{eff}}(n)]/dn$ for the SLM. It should be noted that the determined polarization parameters ($\delta_{\text{eff}}(n)$, $\psi_{\text{eff}}(n)$ and $\delta_{\text{tot}}(n)$) and the corresponding estimates for the dynamical and the PB geometric phases are subject to small
Uncertainties (deviation from ideal values) due to the various approximations used in the theoretical model. Never-the-less, this extremely small spatial gradient of total phase for input LCP state \( \Phi - \frac{\partial}{\partial x} \) did not lead to measurable shift in the beam centroid for input LCP state (Fig. 2), which provides experimental support towards the validity of the theoretical model. Comparison of the experimental momentum domain beam shifts for the input RCP state and the corresponding theoretical predictions (using the results of Fig. 3c in eq. 5) shows reasonable agreement (Fig. 3d). For the theoretical predictions, an approximated linear dependence of \( \Phi + \frac{\partial}{\partial x} \) with \( n \) (for \( n \approx 30-170 \) in Fig. 3c) was assumed and the spatial dimensions (over which the grey levels were applied) were duly considered (the values of the spatial gradients \( \Phi + \frac{\partial}{\partial x} \) noted in Fig. 2 are based on this approximation). Incorporation of the exact dependence of \( \Phi + \) did not lead to significant differences in the predicted trends and absolute values. These results provide concrete evidence of the underlying principle–while for input RCP state, the accumulation of the spatial gradients of the dynamical and the geometrical phases lead to a large shift of the beam-centroid, the spatial gradients nearly cancel out to yield no appreciable shift for the input LCP state.

**Spin dependent splitting of input linearly polarized light beam.** The spin dependent beam shift is usually manifested as a spin dependent splitting of input linearly polarized beam. Like in photonic SHE, the constituent two orthogonal circular polarization modes evolve in different trajectories, leading to a large (and tunable) spin separation (shown in Fig. 4a). Figure 4a displays the transverse momentum distribution \( \pi k_x^2/(\mu m - 1) \) of the transmitted beam (for input linearly polarized beam) after passing through the left (LCP) and right (RCP) circular analyzers. As can be seen, while the constituent RCP mode (noted as \( \sigma^+ \)) experiences a large and tunable momentum domain shift (manifested as a shift of the beam centroid in the detection plane, shown in the bottom panel of Fig. 4a), the other orthogonal mode (LCP, \( \sigma^- \), top panel) evolves in the same trajectory. The spin dependent splitting of input linearly polarized light is evident in the spatial distribution of the circular polarization descriptor Stokes Vector element \( V/I \) (\( V \) is the difference in intensities between the RCP and LCP components and \( I \) is the sum of the two, the total intensity).

**Figure 4.** (a) Spin dependent splitting of input linearly polarized light in an inhomogeneous anisotropic medium exhibiting nearly equal spatial gradient of geometric and dynamical phases. One of the constituent circular polarization mode (RCP, noted as \( \sigma^+ \)) experiences a large and tunable momentum domain shift (manifested as a shift of the beam centroid in the detection plane, shown in bottom panel), the other orthogonal mode (LCP, \( \sigma^- \), top panel) evolves in the same trajectory. The results are displayed for a spatial gradient of the total phase \( \Phi + \frac{\partial}{\partial x} = 9.95 \times 10^{-4} \text{rad/\mu m} \) (as experienced by the RCP mode). (b) The spin separation is shown by the spatial distribution of the circular polarization descriptor Stokes Vector element \( V/I \) (\( V \) is the difference in intensities between the RCP and LCP components and \( I \) is the sum of the two, the total intensity).
polarization descriptor Stokes Vector element \( V \left( \frac{\Delta n(x,y)}{\Delta n + 1/2} \right) \) (Fig. 4b), which shows spatially separated regions of opposite circular polarization states. We note that this spin dependent beam shift is perfectly discernible from other variants of SHE1–6,8,9,14,24 in that (a) only one circular polarization mode experiences the shift, the other orthogonal mode evolves in the same trajectory, (b) the magnitude as well as the direction of the splitting is completely tunable. Moreover, unlike other variant of the momentum domain beam shifts (angular Goos–Hänchen and the angular Imbert–Fedorov shifts16,25), the shift is independent of the beam waist parameter and is exclusively determined by the dynamical and the geometric phase gradients.

To summarize, we have observed an interesting manifestation of spin dependent momentum domain beam shift of light and demonstrated its tunability in an inhomogeneous anisotropic medium. The effect is manifested as a shift of the beam centroid for one circular polarization mode whereas the other orthogonal mode remains unaffected and evolves in the same trajectory. This is shown to arise due to the combined spatial gradients of the PB geometric phase and dynamical phase of light. It is pertinent to emphasize here that the SOI and the SHE effects in inhomogeneous anisotropic medium reported so far, deal with systems having spatially varying axis of retardance (and with constant magnitude of retardance), which leads to generation of space varying geometric phase alone18,25,26. In contrast, as demonstrated here, if one introduces a spatially varying magnitude of retardance, one may simultaneously generate space varying PB geometric phase and dynamical phase of light in a regulated manner to produce momentum domain beam shift for one circular polarization mode only. While the effect is demonstrated in a twisted nematic liquid crystal-based system, albeit with a relatively smaller spatial gradient (limited by the spatial dimension of the pixels), the principle can be extended to a wide class of anisotropic nano-optical systems25,6,7,26–28, wherein the phase gradients can be enhanced by several orders of magnitude to produce giant spin dependent beam shift. For example, space varying anisotropy effects can be tailored in specially designed plasmonic nano structures24,26,28–30 to produce such effects. We are currently expanding our investigations in this direction. In general, the remarkable simplicity of the approach of simultaneously tailoring spatial gradient of geometric and dynamical phases of light to produce such dramatic spin dependent beam shift may provide an attractive route towards development of spin-controlled photonic devices for the generation, manipulation and detection of spin-polarized photons.

Methods

A schematic of the experimental system is shown in Fig. 1. Fundamental Gaussian (TEM\(_{00}\)) mode of 632.8 nm line of a He–Ne laser (HRR120-1, Thorlabs, USA), is spatially filtered, collimated (using Lens, Pinhole and aperture assembly), and made incident on a transmissive spatial light modulator (SLM). The transverse momentum distribution \((k_x, k_y, and k_z)\) of the transmitted beam is imaged into a CCD camera (Micro Publisher 3.3, Qimaging, 2048 x 1536 square pixels, pixel dimension 3.45 \(\mu m\)). The polarization state generator (PSG) and the polarization state analyzer (PSA) units are used to generate and analyze desirable polarization states of light. The PSG unit comprises of a fixed Glan-Thompson linear polarizer (\(P_0\), GTH10M, Thorlabs, USA) and a rotatable quarter waveplate (QWP\(_0\), WPQ10M-633, Thorlabs, USA) mounted on a computer-controlled rotational mount (PRM1/ MZ8, Thorlabs, USA). The PSA unit essentially consists of a similar arrangement of fixed linear polarizer (\(P_0\)) and a rotatable quarter waveplate (QWP\(_0\)), but positioned in a reverse order.

In order to observe tunable spin specific beam shift and spin-dependent splitting of light beam, the inhomogeneous anisotropic medium (having spatially varying birefringence level) was realized by modulating the pixels of the SLM by user controlled grey level \((n)\) distributions. Desirable grey level gradient was created along one chosen linear direction \((x or y)\) by using a range of grey level values between \(n=30\) to \(170\). For this range the grey level gradient of the total retardance parameter was nearly equal to the corresponding gradient of the effective optical rotation parameter \((\ast \ast)\). This choice of the range of \(n\) enabled us to produce equal spatial gradients of the dynamical and the PB geometric phases in the SLM by creating grey level gradient in the SLM along one chosen linear direction \((x or y)\). Variable spatial gradient of grey levels was achieved by accommodating this within variable spatial dimensions \((\Delta x=2.144\, \text{mm} \approx 6.816\, \text{mm}, \text{limited by the beam spot size and the transverse width of the SLM})\) of the relayed image to the SLM. Since, the spatial dimension \(\Delta x\) was varied in equal steps keeping the total range of phase \((\Delta \Phi^\text{tot}) \approx 5897\, \text{rad}, \text{corresponding to} n=30\) to \(170\), Fig. 3c) fixed, the spatial gradient of the total phase \(\frac{\Delta \Phi^\text{tot}}{\Delta x}\) was not changed in equal steps (as apparent from Fig. 3d). While studying the spin specific beam shift, the PSA unit was removed and the PSG unit was used to sequentially generate RCP and LCP polarization states. For observing the spin-dependent splitting of light, the PSG unit was used to sequentially generate RCP and LCP polarization states. For observing the spin-dependent splitting of light, the PSG unit was used to sequentially generate RCP and LCP polarization states. For observing the spin-dependent splitting of light, the PSG unit was used to sequentially generate RCP and LCP polarization states.
measurements (images) were performed by sequentially changing the orientation of the fast axis of the quarter waveplates of the PSG unit and that of the PSA unit, to four optimized angles 35°, 70°, 105° and 140° (representing four optimized generator elliptical basis states and corresponding four analyzer basis states) (see Supplementary Information). During these measurements, the axis of the polarizer (P_1) in the PSG was fixed along the laboratory horizontal direction and that (P_2) in the PSA was kept along the laboratory vertical direction. These sixteen intensity measurements were then combined to generate the system Mueller matrix following the approach described in ref. 30. Eigenvalue calibration of the system ensured high accuracy of Mueller matrix measurement (accuracy ~0.01 in normalized matrix elements)30.

References

1. Blokh, K. Y., Niv, A., Kleiner, V. & Hasman, E. Geometrodynamics of spinning light. Nat. Photon. 2, 748–753 (2008).
2. Rodríguez-Herrera, O. G., Lara, D., Blokh, K. Y., Ostrovskaya, E. A. & Dainty, C. Optical nanoprobing via spin-orbit interaction of light. Phys. Rev. Lett. 104, 253601 (2010).
3. Hosten, O. & Kwiat, P. Observation of the spin Hall effect of light via weak measurements. Science 319, 787–790 (2008).
4. Aiello, A., Lindein, N., Marquardt, C. & Leuchs, G. Transverse Angular Momentum and Geometric Spin Hall Effect of Light. Phys. Rev. Lett. 103, 100401 (2009).
5. Zhou, X., Ling, X., Luo, H. & Wen, S. Identifying graphene layers via spin Hall effect of light. Appl. Phys. Lett. 101, 251602 (2012).
6. Yin, X., Ye, Z., Rho, J., Wang, Y. & Zhang, X. Photonic Spin Hall Effect at Metasurfaces. Science 339, 1045–1047 (2013).
7. Shtrit, N. et al. Spin Optical Metamaterial Route to Spin-Controlled Photonics. Science 340, 724–726 (2013).
8. Zhou, X., Xiao, Z., Luo, H. & Wen, S. Experimental observation of the spin Hall effect of light on a nanometal film via weak measurements. Phys. Rev. A 85, 043809 (2012).
9. Ling, X. et al. Giant photonic spin Hall effect in momentum space in a structured metamaterial with spatially varying birefringence. Light: Science and Applications 4, e299 (2015).
10. Blokh, K. Y. & Aiello, A. Goos–Hänchen and Imbert–Fedorov beam shifts: an overview. J. Optics 15, 014001 (2013).
11. Simon, R., Kimble, H. J. & Sudarshan, E. C. G. Evolving Geometric Phase and Its Dynamical Manifestation as a Frequency Shift: An Optical Experiment. Phys. Rev. Lett. 61, 19–22 (1988).
12. Bretenaker, F. & Floch, L. Energy exchanges between a rotating retardation plate and a laser beam. Phys. Rev. Lett. 65, 2316 (1990).
13. Korech, O., Steinitz, U., Gordon, R. J., Averbukh, I., Sh. & Prior, Y. Observing molecular spinning via the rotational Doppler effect. Nat. Photon. 7, 711–714 (2013).
14. Blokh, K. Y., Gorodetski, Y., Kleiner, V. & Hasman, E. Coriolis Effect in Optics: Unified Geometric Phase and Spin-Hall Effect. Phys. Rev. Lett. 101, 030404 (2008).
15. Marrucci, L., Manzo, C. & Paparo, D. Optical Spin-to-Orbital Angular Momentum Conversion in inhomogeneous Anisotropic Media. Phys. Rev. Lett. 96, 163905 (2006).
16. Andrews, D. L. & Babiker, M. The Angular momentum of Light Ch. 8 (Cambridge University Press, 2013).
17. Lu, K. & Saleh, B. E. A. Theory and design of the liquid crystal TV as an optical spatial phase modulator. Opt. Eng. 29, 240–246 (1990).
18. Durán, V., Lancia, J., Tajahuerce, E. & Jarsowezicz, Z. Cell parameter determination of a twisted-nematic liquid crystal display by single-wavelength polarimetry. J. Appl. Phys. 97, 043101 (2005).
19. Gutiérrez-Vega, J. C. Pancharatnam–Berry phase of optical systems. Opt. Lett. 36, 1143–1145 (2011).
20. Berry, M. V. The adiabatic phase and Pancharatnam’s phase for polarized light. J. Mod. Optics 34, 1401–1407 (1987).
21. Dijk, T. V., Schouten, H. F. & Visser, T. D. Geometric interpretation of the Pancharatnam connection and non-cyclic polarization changes. J. Opt. Soc. Am. A 27, 1972–1976 (2010).
22. Goldstein, D. Polarized Light (Taylor & Francis Inc, 2003).
23. Lu, S. & Chipman, R. A. Interpretation of Mueller matrices based on polar decomposition. J. Opt. Soc. Am. A 13, 1106–1113 (1996).
24. Shtrit, N., Brentner, I., Gorodetski, Y., Kleiner, V. & Hasman, E. Optical Spin Hall Effects in Plasmonic Chains. Nano Lett. 11, 2038–2042 (2011).
25. Merano, M., Aiello, A., Exter, M. P. V. & Woerdman, J. P. Observing angular deviations in the specular reflection of a light beam. Nat. Photon. 3, 337–340 (2009).
26. Gorodetski, Y., Drezet, A., Genet, C. & Ebbesen, T. W. Generating far-field optical vortices from near-field optical Chirality. Phys. Rev. Lett. 110, 203906 (2013).
27. Lin, D., Fan, P., Hasman, E. & Brongersma, M. L. Dielectric gradient metasurfaces optical elements. Science 345, 298–302 (2014).
28. Mezina, N., Barnes, W. L. & Hooper, I. R. Plasmonic meta-atoms and metasurfaces. Nat. Photon. 8, 889–898 (2014).
29. Gorodetski, Y., Lombard, E., Drezet, A., Genet, C. & Ebbesen, T. W. A perfect plasmonic quarter-wave plate. Appl. Phys. Lett. 101, 201103 (2012).
30. Soni, J. et al. Enhancing spin-orbit interaction of light by plasmonic nanostructures. Opt. Lett. 38, 1748–1750 (2013).
31. Chipman, R. A. Handbook of Optics Vol. 2 (eds Bass, M.) Ch. 22, 22.1–22.37, 2nd ed. (McGraw-Hill, 1994).
32. Soni, J. et al. Quantitative fluorescence and elastic scattering tissue polarimetry using an Eigenvalue calibrated spectroscopic Mueller matrix system. Opt. Exp. 21, 15475–15489 (2013).

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Author Contributions

M.P. and C.B. performed all the experiments, analyzed data, contributed in theoretical modeling and in writing the manuscript. S.C. contributed in designing experimental strategies and in performing the experiments. A.B. contributed in performing the experiments and in analysis/interpretation of data. S.K.M. contributed in data analysis/interpretation and in writing the manuscript. N.G. designed and supervised this study; contributed in writing the manuscript, designing experimental strategies and theoretical models, contributed in analysis/interpretation of the results.

Additional Information

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