Galactic evolution of rapid neutron capture process abundances: the inhomogeneous approach

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ABSTRACT
For the origin of heavy rapid neutron capture process (r-process) elements, different sources have been proposed, e.g. core-collapse supernovae or neutron star mergers. Old metal-poor stars carry the signature of the astrophysical source(s). Among the elements dominantly made by the r-process, europium (Eu) is relatively easy to observe. In this work we simulate the evolution of Eu in our Galaxy with the inhomogeneous chemical evolution (ICE) model, and compare our results with spectroscopic observations. We test the most important parameters affecting the chemical evolution of Eu: (a) for neutron star mergers the coalescence time-scale of the merger (t_{coal}) and the probability to experience a neutron star merger event after two supernova explosions occurred and formed a double neutron star system (P_{NSM}), and (b) for the subclass of magnetorotationally driven supernovae (‘Jet-SNe’), their occurrence rate compared to standard supernovae (P_{Jet-SN}). We find that the observed [Eu/Fe] pattern in the Galaxy can be reproduced by a combination of neutron star mergers and Jet-SNe as r-process sources. While neutron star mergers alone seem to set in at too high metallicities, Jet-SNe provide a cure for this deficiency at low metallicities. Furthermore, we confirm that local inhomogeneities can explain the observed large spread in the Eu abundances at low metallicities. We also predict the evolution of [O/Fe] to test whether the spread in α-elements for inhomogeneous models agrees with observations and whether this provides constraints on supernova explosion models and their nucleosynthesis.

Key words: nuclear reactions, nucleosynthesis, abundances – Galaxy: abundances – Galaxy: evolution.

1 INTRODUCTION
The rapid neutron capture process (r-process; e.g. Thielemann et al. 2011, and references therein) is responsible for the production of about half of the heavy element abundances beyond Fe in the Solar system, and of the heaviest elements like Th and U. The remaining heavy element abundances are mostly made by the slow neutron capture process (s-process; e.g. Käppeler et al. 2011). Despite its relevance, the true astrophysical origin of the r-process is still under debate. Because of the larger uncertainties affecting the r-process nucleosynthesis predictions compared to the s-process in stars, the r-process isotopic contribution in the Solar system has been originally identified by using the residual method, i.e. by subtracting the s-process component from the solar isotopic distribution (e.g. Arlandini et al. 1999; Bisterzo et al. 2014). The r-process residual abundances have been shown to be consistent in first approximation with the abundance signatures in old r-process rich metal-poor stars (at least for elements heavier than Ba; see Travaglio et al. 2004 for details), carrying the signature of the r-process nucleosynthesis in the early Galaxy (e.g. Sneden, Cowan & Gallino 2008). For instance, europium (Eu) receives only a marginal contribution from the s-process (the s-process explains only 6 per cent of the solar Eu, while the remaining amount has an r-process origin; Bisterzo et al. 2014), and therefore it is often used as a tracer of the r-process nucleosynthesis in stellar spectroscopic observations. One possibility to test predictions from r-process nucleosynthesis is to include the r-process stellar yields in galactic chemical evolution (GCE) simulations, and to compare the theoretical results with spectroscopic observations at different metallicities. Eu is an ideal diagnostic for these studies. The purpose of this work is to illustrate the Eu evolution throughout the evolution of our Galaxy. We consider here the contribution from two sites (and their frequency) to the production of heavy r-process elements: Neutron star merger (NSM) and ‘magnetorotationally driven supernovae’ (hereafter referred to as ‘Jet-SNe’). We will show that the combination of both sites is able

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to reproduce the observed Eu abundance distribution of the stars of our Galaxy.

Neutron star–black hole (NS–BH) mergers might have a non-negligible contribution to the r-process inventory in the Galaxy. However, their relevance as astrophysical source for the r-process is controversial, since this event has not yet been observed (e.g. Bauswein et al. 2014). These difficulties also result in an extreme divergence of the predicted galactic rate of such an event (e.g. Postnov & Yungelson 2014). However, it should be noticed that a contribution from NS–BH mergers has been predicted as well (e.g. Korobkin et al. 2012; Memmekens & Vanbeveren 2014). We give an estimate of the possible effects caused by these events in Section 5.

Chemical evolution of galaxies has made strong advances since its early days. Initially all approaches made use of the instantaneous recycling approximation in the sense that the ejecta of stellar end stages were immediately utilized without delay after the initial star formation, assuming that the stellar evolution time-scale is short in comparison to galactic evolution. If, in addition, the instantaneous mixing approximation (IMA) was applied, i.e. assuming that the ejecta were instantaneously mixed throughout the galaxy, the whole galaxy acts as a homogeneous box. Neglecting this can explain radial gradients. Further developments included infall of primordial matter into and outflow of enriched material out of the galaxy (for a review of these early investigations see e.g. Audouze & Tinsley 1976). When relaxing the instantaneous recycling approximation, i.e. taking into account that (explosive) stellar ejecta enter the interstellar medium (ISM) delayed with respect to the birth of a star by the duration of its stellar evolution, detailed predictions for the evolution of element abundances can be made. Based on nucleosynthesis predictions for stellar deaths, a number of detailed analyses have been performed, from light elements up to the Fe group (e.g. Timmes et al. 1995; Goswami & Prantzos 2000; Matteucci 2001, 2012; Gibson et al. 2003; Kobayashi et al. 2006; Pagel 2009; Kobayashi 2012). Such approaches have recently also been applied to understand the enrichment of heavy elements in the Galaxy (including r-process contributions) as a function of time or metallicity [Fe/H] (see e.g. Ishimaru & Wanajo 1999; Travaglio et al. 1999; De Donder & Vanbeveren 2003; Matteucci 2012; Vangioni et al. 2015).

However, if still the IMA is applied, i.e. such ejecta are instantaneously mixed with the global ISM, no local inhomogeneities can be produced. The latter would relate to the fact that only limited amounts of the ISM are polluted by the ejecta of each event. This effect is of essential importance, especially at low metallicities, where portions of the ISM are already polluted by stellar winds and supernovae, and others are not. In addition, different portions of the ISM are polluted by different types of events, leading to a scatter at the same metallicity, which can in fact be utilized as a constraint for these different stellar ejecta. When, however, utilizing the IMA, this leads to a unique relation between galactic evolution time and metallicity [Fe/H], i.e. any [Fe/H] can be related to a specific time in the evolution of a galaxy (while inhomogeneous mixing could experience similar [Fe/H] values in different locations of the galaxy at different times). This is especially the case in the very early galactic evolution ([Fe/H] < −2.5), when locally only a few stars [out of a whole initial mass function (IMF)] might have exploded and imprinted their stellar neighbourhood with their ejecta. Thus, the application of chemical evolution models which utilize the IMA is questionable for the early evolution of galaxies.

In addition, for each [Fe/H], due to the instantaneous mixing, only a mean value of [X/Fe] (X being the element of interest to follow in chemical evolution) is obtained. Inhomogeneous mixing, however, could produce larger ratios in strongly polluted areas and smaller values in still less polluted ones. This means that the scatter in [X/Fe] at low metallicities, which might also be a helpful asset in pointing to the origin of element X, cannot be reproduced or utilized with a homogeneous treatment. In the case of rare events, which – on the other hand – produce large amounts of element X in each event, this would produce a large scatter, and – if observed – could be used as a very helpful constraint to identify the production site. For these reasons, especially for the origin of r-process elements like Eu, we think that only inhomogeneous chemical evolution models should be utilized at low metallicities. The two type of rare events (i) Jet-SNe [maybe up to 1 per cent of all core-collapse supernovae (CCSNe)] and (ii) NSMs, with a similar occurrence frequency of about 1 per cent of all CCSNe, are considered here, while regular and more frequent CCSNe might at most contribute to the lighter r-process elements. The binary merger rates are estimated by van den Heuvel & Lorimer (1996) and Kalogera et al. (2004). The rate of Jet-SNe is related to the fact that about 1 per cent of neutron stars are found with magnetic fields of the order 10¹⁵ G (magnetars, see e.g. Kouveliotou et al. 1998; Kramer 2009).

Earlier inhomogeneous chemical evolution models for r-process elements like Eu have been provided by Travaglio, Galli & Burkert (2001, where the r-process yields were assumed to come from CCSN), Argast et al. (2004), and Matteucci et al. (2014) comparing NSMs and CCSNe, Cescutti & Chiappini (2014, comparing NSM and Jet-SNe), Mennekens & Vanbeveren (with NSM and NS–BH mergers), and Shen et al. (2015) and van de Voort et al. (2015, only utilizing NSMs). One of the main questions here is related to the problem of reproducing [Eu/Fe] at low(est) metallicities. Cescutti & Chiappini (2014) have shown that this is possible with Jet-SNe. Argast et al. (2004) concluded that NSMs cannot reproduce observations at [Fe/H] < −2.5, while van de Voort et al. (2015) and Shen et al. (2015) came to the opposite conclusion.

The main difference between Jet-SNe and NSMs is that in one case the immediate progenitors are massive stars and the first occurrence in chemical evolution is due to the death of massive stars. In the other case the progenitors are also massive stars, leading to two supernova explosions in a binary system, which – if not disrupted – causes a binary neutron star system and a merger with a given delay time due to gravitational radiation losses. Thus, one needs to consider two aspects: (i) the two supernova explosions and the pollution of the ISM with their ejecta (for the case of NS–BH mergers see the discussion in Section 5), and (ii) the delay time of the merger event after the formation of the binary neutron star system. Especially aspect (i) can only be treated adequately with inhomogeneous evolution models, and there an additional factor is of major importance: with how much matter the supernova ejecta mix before the NSMs eject their products into the same environment.

This paper is organized as follows. In Section 2, we introduce the model used to compute the evolution of abundances. In Section 3, we present the influence of the different r- and non-r-process sites on the evolution. Additionally, we provide an overview why an inhomogeneous treatment of the evolution is important. In Section 4 we discuss the impact of inhomogeneities, causing and permitting a scatter of [X/Fe] ratios at low metallicities. As a further test of the model, we discuss the fact why the large scatter of [r/Fe] observed at low metallicities is strongly reduced for α-elements, and show how this constraints CCSNe nucleosynthesis predictions, which are still not available in a self-consistent way. In Section 5, our results are summarized and discussed.
Table 1. Main infall parameters. See Argast et al. (2004) for details on the parameters.

| $M_{\text{tot}}$ | Total infall mass | $10^8 \, M_{\odot}$ |
|------------------|------------------|-------------------|
| $\tau$          | Time-scale of infall decline | $5 \times 10^8$ yr |
| $t_{\text{max}}$ | Time of the highest infall rate | $2 \times 10^8$ yr |
| $t_{\text{final}}$ | Duration of the simulation | $13.6 \times 10^8$ yr |

2 THE MODEL

Recent chemodynamical galactic evolution models, like e.g. Minchev, Chiappini & Martig (2014), van de Voort et al. (2015), and Shen et al. (2015), can model in a self-consistent way massive mergers of galactic subsystems (causing effects like infall in simpler models), energy feedback from stellar explosions (causing effects like outflows), radial migrations in disc galaxies, mixing and diffusion of matter/ISM, and the initiation of star formation dependent on local conditions, resulting from the effects discussed above. In our present investigation we still utilize a more classical approach with a parametrized infall of primordial matter, and a Schmidt law (Schmidt 1959) for star formation. Therefore, we neglect large-scale mixing effects, while we include the feedback from stellar explosions and the resulting mixing with the surrounding ISM, according to a Sedov–Taylor blast wave. In this way, the model permits to keep track of the local inhomogeneities due to different CCSN ejecta. This approach allows us to grasp the main features of the impact of the first stars/stellar deaths on the evolution of the heavy element enrichment. This approximation omits other mixing effects, e.g. spiral arm mixing (on time-scales of the order of $2 \times 10^8$ yr). The main focus of this work is the investigation of the chemical evolution behaviour at low metallicities, where these effects should not have occurred, yet, and are therefore left out in this first-order approximation.

We treat the GCE of Eu, Fe, and $\alpha$-elements (e.g. oxygen), utilizing the established GCE code ICE, created by Argast et al. (2004). A detailed description of the model can be found therein.

For the simulation, we set up a cube of $(2 \, \text{kpc})^3$ within the galaxy which is cut in $40^3$ smaller cubes representing a $(50 \, \text{pc})^3$ subcube each. The evolution is followed with time steps of 1 Myr. Primordial matter is assumed to fall into the simulation volume, obeying the form

$$\dot{M}(t) = a \, t^b \, e^{-t/\tau},$$

which permits an initially rising and eventually exponentially declining infall rate. While $\tau$ and the total galaxy evolution time $t_{\text{final}}$ are fixed initially, the parameters $a$ and $b$ can be determined alternatively from $M_{\text{tot}}$ (the total infall mass integrated over time), defined by

$$M_{\text{tot}} := \int_0^{t_{\text{final}}} a \, t^b \, e^{-t/\tau},$$

and the time of maximal infall $t_{\text{max}}$ given by

$$t_{\text{max}} := b \, \tau.$$  

See Argast et al. (2004) for an extended discussion of the infall model and Table 1 for the applied parameters.

2.1 Treating stellar births and deaths

The main calculation loop at each time step (1 Myr) can be described in the following way.

(i) We scan all mass cells of the total volume and calculate the star formation rate per volume and time step ($10^9$ yr) according to a Schmidt law with a density power $\alpha = 1.5$ (see Schmidt 1959; Larson 1991; Kennicutt 1998). Dividing by the average stellar mass of a Salpeter IMF (power $−2.35$) provides the total number of stars per time step $n(t)$ created in the overall volume of our simulation.

(ii) Individual cells in which stars are formed are selected randomly until $n(t)$ is attained, but the probability is scaled with the density, which leads to the fact that patches of higher density, predominantly close to supernova remnants, are chosen.

(iii) The mass of a newly created star is chosen randomly in the range $0.1−50 \, M_{\odot}$, subject to the condition that the mass distribution of all stars follows a Salpeter IMF. Consequently only cells which contain more than $50 \, M_{\odot}$ are selected in order to prevent a bias.

(iv) The newly born star inherits the composition of the ISM out of which it is formed.

(v) The age of each star is monitored, in order to determine the end of its lifetime, either to form a white dwarf or experience a supernova explosion (see Sections 2.2.1 and 2.2.2). A fraction of all high-mass stars (HMS; $M > 8 \, M_{\odot}$), according to the probability ($P_{\text{SN}}$), are chosen to undergo a Jet-SN event (see Section 3.2). Type Ia supernova (SNla) events are chosen from white dwarfs according to the discussion in Section 2.2.3. The treatment of NSMs follows the description in Section 2.2.4.

(vi) The composition for the ejecta of all these events is chosen according to the discussion in Section 2.2. They will pollute the neighbouring ISM with their nucleosynthesis products and sweep up the material in a chemically well-mixed shell. We assume that an event pollutes typically $5 \times 10^4 \, M_{\odot}$ of surrounding ISM due to a Sedov–Taylor blast wave of $10^{51}$ erg (Ryan, Norris & Beers 1996; Shigeyama & Tsujimoto 1998). This implies that the radius of a remnant depends strongly on the local density and the density of the surrounding cells.

(vii) In the affected surrounding cells, stars are polluted by the matter of the previously exploded star and the event-specific element yields.

The details on the above procedure will be explained in the following.

2.2 Nucleosynthesis sites

2.2.1 Low- and intermediate-mass stars

Low- (LMS) and intermediate-mass stars (IMS) provide a fundamental contribution to the GCE of e.g. He, C, N, F, Na, and heavy s-process elements during the asymptotic giant branch (AGB) phase. For instance, most of the C and N in the Solar system were made during the AGB phase, these stars lock-up a part of the overall mass and return most of it to the ISM in their AGB phase by stellar winds. Since the maximum radius of these winds is orders of magnitude smaller than the output range of supernova events (e.g. radius of Crab Nebula remnant is 5.5 light-year, Hester 2008), while the diameter of the Cat’s Eye Nebula is only 0.2 light-year, Reed et al. 1999), our simulation assumes that stellar winds influence the ISM only in the local calculation cell. AGB stars provide only a marginal s-process contribution to typical r-process elements like Eu (e.g. Travaglio et al. 1999). In particular, for this work the s-process contribution to Eu plays a negligible role and we are not considering it here.
2.2.2 High-mass stars

Massive stars which exceed $8 \, M_\odot$ are considered to end their life in a CCSN (e.g. Thielemann, Nomoto & Hashimoto 1996; Nomoto et al. 1997; Woosley, Heger & Weaver 2002; Jones et al. 2013; Nomoto, Kobayashi & Tominaga 2013). CCSNe produce most of the O and Mg in the chemical inventory of the galaxy. They provide an important contribution to other $\alpha$-elements (S, Ca, Ti), to all intermediate-mass elements, the iron-group elements, and to the s-process species up to the Sr neutron-magic peak (e.g. Rauscher et al. 2002). Associated to CCSNe, different neutrino-driven nucleosynthesis components might be ejected and contribute to the GCE (e.g. Arcones & Thielemann 2013, and references therein), possibly including the r-process. We did not include regular CCSNe as a major source of heavy r-process elements, as recent investigations indicate strongly that the early hopes for a high entropy neutrino wind with the right properties (Takahashi, Witti & Janka 1994; Woosley et al. 1994) did not survive advanced core collapse simulations (e.g. Liebendörfer et al. 2003) which led to proton-rich environments in the innermost ejecta (see also Fischer et al. 2010; Hüdepohl et al. 2010), causing rather a so-called vp-process (Pruet et al. 2005, 2006; Fröhlich et al. 2006a,b; Wanajo 2006). Further investigations seem to underline this conclusion (recently revisited by Wanajo 2013), although a more advanced – in medium – treatment of neutrons and protons in high-density matter causes possible changes of the electron fraction ($Y_e$) of ejecta (Roberts et al. 2011; Martínez-Pinedo et al. 2012) and might permit a weak r-process, including small fractions of Eu. Similar effects might be possible via neutrino oscillations (Wu et al. 2015). For this reason we did not include regular CCSNe in our GCE simulations, although a weak r-process with small (Honda et al. 2006) Eu contributions could be responsible for a lower bound of [Eu/Fe] observations (see Fig. 5), explaining a non-detection of the lowest predicted [Eu/Fe] ratios. Nucleosynthesis yields for HMS are taken from Thielemann et al. (1996) or Nomoto et al. (1997). Assuming a typical explosion energy of $10^{51}$ erg, the ejecta are mixed with the surrounding ISM via the expansion of a Sedov–Taylor blast wave, which stops at a radius which contains about $5 \times 10^4 M_\odot$ (see Section 2.1 for details on the iteration procedure).

2.2.3 Type Ia supernovae

When an IMS is newly born in a binary system, there is a probability that it has a companion in the appropriate mass range leading finally to a SN II, following a double- or single-degenerate scenario. We follow the analytical suggestion of Greggio (2005) and reduce the numerous degeneracy parameters to one probability ($P_{\text{SNII}} = 9 \times 10^{-4}$) for a newly born IMS to actually be born in a system fulfilling the prerequisites for a SNII. Once the star enters its red giant phase, we let the system performs a SNII-type explosion and emits the event-specific yields (cf. Iwamoto et al. 1999, model CDD2), which highly enriches the surrounding ISM with iron. For this work we use the same SNII yields for each metallicity, consistently with the Argast et al. (2004) calculations. We are aware that this choice is not optimal, since several SNII yields including e.g. Mn and Fe depend on the metallicity of the SNII progenitor (e.g. Timmes, Brown & Truran 2003; Thielemann et al. 2004; Travaglio, Hillebrandt & Reinecke 2005; Bravo et al. 2010; Seitenzahl et al. 2013). On the other hand, this approximation does not have any impact on our analysis and our conclusions.

2.2.4 Neutron star merger

If two newly born HMS were created in a binary system, they may both undergo a CCSN individually. This could leave two gravitationally bound neutron stars (‘NS’) behind. Such a system emits gravitational waves and the two NS spiral inwards towards their common centre of mass with a coalescence time ($t_{\text{coa}}$) until they merge. The actual merging event is accompanied by an ejection of matter and (r-process) nucleosynthesis (Freiburghaus, Rosswog & Thielemann 1999; Panov, Korneev & Thielemann 2008; Korobkin et al. 2012; Bauswein, Goriely & Janka 2013; Rosswog 2013; Rosswog et al. 2014; Wanajo et al. 2014; Eichler et al. 2015). As all of these publications show the emergence of a strong r-process, in the mass region of Eu they suffer partially from nuclear uncertainties related to fission fragment distributions (see e.g. Goriely et al. 2013; Eichler et al. 2015). For our purposes we chose to utilize as total amount of r-process ejecta $1.28 \times 10^{-2} M_\odot$ (consistent with the 1.4 $+ 1.4 M_\odot$ NS collision in Korobkin et al. 2012; Rosswog 2013), but distributed in solar r-process proportions, which leads for Eu to a total amount of $10^{-4} M_\odot$ per merger. This value is relatively high in comparison to other investigations in the literature.

Observational constraints for the probability of a newly born star to undergo this procedure ($P_{\text{NSM}}$) are provided by e.g. Kalogera et al. (2004) who have found a NSM rate of $\dot{P}_{\text{NSM}} = 83.0^{+309.1}_{-661}$ Myr$^{-1}$, which corresponds to a $P_{\text{NSM}} = 0.0180^{+0.0453}_{-0.0143}$. The coalescence time, $t_{\text{NSM}}$, and the event-specific yields are important parameters for GCE, and their influence on the GCE are subject of this paper. Concerning the coalescence time-scale, it might be more realistic to use a distribution function (e.g. as in Ishimaru, Wanajo & Prantzos 2015) instead of a fixed value. We utilize this simplified procedure as a first-order approach.

2.2.5 Magnetorotationally driven supernovae

A fraction ($P_{\text{Jet-SN}}$) of HMS end their life as a ‘Jet-SN’ or magnetar, forming in the centre a highly magnetized neutron star (with fields of the order $10^{15}$ G) and ejecting r-process matter along the poles of the rotation axis (Fujimoto et al. 2006; Fujimoto, Nishimura & Hashimoto 2008; Winteler et al. 2012; Mösta et al. 2014). r-process simulations for such events were first undertaken in 3D by Winteler et al. (2012). For the purpose of this work, we randomly choose newly born HMS to later form a Jet-SN. At the end of their lifetime, they explode similar to a CCSN, however with different ejecta. Based on Winteler et al. (2012), we assume an amount of $14 \times 10^{-5} M_\odot$ of Eu ejected to the ISM by such an event. In this work, we study the influence of $P_{\text{Jet-SN}}$ and the specific Jet-SN yields on the GCE.

2.3 Observed stellar abundances

Data for the observed stars to compare our simulation results with are taken from the Stellar Abundances for Galactic Archaeology (SAGA) data base (e.g. Suda et al. 2008, 2011; Yamada et al. 2013; in particular [Eu/Fe] abundance observations are mainly from e.g. Shetrone, Côté & Stetson 2001; McWilliam, Wallerstein & Mottini 2003; Shetrone et al. 2003; Simmerer et al. 2004; Barklem et al. 2005; Geisler et al. 2005; Francois et al. 2007; Cohen & Huang 2009; Letarte et al. 2010; Roederer et al. 2010, 2014a,b,c; Rafelski et al. 2012; Starkenburg et al. 2013). From the raw data, we excluded carbon enriched metal-poor stars (‘CEMPs’) and stars with binary nature, since the surface abundances of such objects are expected
to be affected by internal pollution from deeper layers or pollution from the binary companion.

3 RESULTS

For a general understanding of the effects of Jet-SNe and NSM on GCE, namely the parameters $P_{\text{NSM}}$, $t_{\text{coal}}$, and $P_{\text{Jet-SN}}$, we performed a number of simulations described in detail below.

3.1 Coalescence time-scale and NSM probability

As a prerequisite, we studied the influence of both coalescence time and the probability of a binary system to become a NSM. In Fig. 1, we present the evolution of [Eu/Fe] abundances when only NSM contribute to the enrichment. The results can be summarized as follows.

(i) Smaller coalescence time-scale leads to an enrichment of Eu at lower metallicities. Larger coalescence time-scale shifts this to higher metallicities.

(ii) A higher NSM probability shifts towards a quantitatively higher enrichment combined with an appearance at lower metallicities.

These effects can be explained in the following way.

(i) When binary neutron star systems take longer to coalesce, the time between the CCSN of both stars and the NSM event is longer. The longer this delay time, also further nucleosynthesis events occur in the galaxy during this period, enriching the ISM with metals. Thus, when the NSM event finally takes place, surrounding stars have developed a higher [Fe/H] abundance, shifting the system towards higher [Fe/H] abundances, respectively. This implies an overall Eu production shift towards higher metallicities.

(ii) With more binary systems becoming NSM, the produced Eu amount per time step is larger, since every event produces the same amount of r-process elements. This leads to a higher [Eu/Fe] abundance, compared to simulations with lower NSM probability.

As the fraction of NSM systems are higher while the CCSN rate is constant, larger amounts of Eu are produced, while the surrounding medium evolves regularly. This also leads to a higher abundance of Eu at lower [Fe/H]. These effects shift the [Eu/Fe] curve to higher values for the same [Fe/H].

All these results are consistent with the earlier conclusions by Argast et al. (2004), stating that it is extremely difficult to reproduce the observed [Eu/Fe] ratios at metallicities [Fe/H] < −2.5 by NSM alone. A potential solution would be that the preceding supernovae which produced the two neutron stars of the merging system mix their ejecta with more extended amounts of the ISM. We utilized the results following a Sedom–Taylor blast wave of $10^{51}$ erg, which pollutes of the order $5 \times 10^5 M_\odot$ of ISM until the shock is stopped. van de Voort et al. (2015) assumed (in their standard case) the mixing with more than $10^6 M_\odot$ of ISM (Shen et al. 2015 utilized $2 \times 10^5 M_\odot$ in a similar approach). This produces an environment with a substantially lower [Fe/H] into which the NSM ejecta enter. Thus, it is not surprising that in such a case the Eu enrichment by NSM is setting in at lower metallicities. The higher resolution run shown in fig. 4 of van de Voort et al. (2015) agrees with our results. Thus, the major question is whether such a very much enlarged mixing with the ISM by almost two orders of magnitude can be substantiated. We will discuss these aspects further in Section 5.

3.2 Probability of Jet-SNe

The contribution of Jet-SNe to the galactic Eu abundance differs from that of NSM. Since Jet-SNe explode directly from a massive star, they contribute much earlier to the chemical evolution than NSM. Since the interstellar matter is distributed more inhomogeneously than in later evolution stages of the galaxy, high [Eu/Fe] abundances are possible in individual stars. This leads to a large spread in the abundances towards lower metallicities. Considering Jet-SNe, the parameter with the highest impact on GCE for such rare events, similar to NSM events but ‘earlier’ in metallicity, is the probability of a massive star to actually become a Jet-SN. A lower probability leads to a smaller overall [Eu/Fe] abundance, while a higher probability leads to larger abundances. However, we also recognize a larger spread in abundances in models with lower probability. This comes from the fact that the high yield of the event only sets an upper limit on the abundances. The rarer an event is, the more and the longer stars remain unpolluted. This results in a larger spectrum of abundances in stars and therefore in a larger spread in [Eu/Fe] ratios. Note from Figs 2 and 3 that Jet-SNe might explain the abundances at low metallicities better than NSM. Thus, while Jet-SNe alone could be an explanation for the lower metallicity observations, there is clear evidence of NSM events and therefore we have to examine the combination of both events. Whether the apparently high concentration of model stars with low [Eu/Fe] values at metallicities $-3 < [\text{Fe/H}] < -2$ in comparison to observations is related to observational bias or whether we require another additional source will be discussed in the following sections.

3.3 Combination of sites

If both sites (Jet-SN and NSM) are considered to contribute to the galactic Eu abundances, their contributions overlap. Therefore, parameters which lead to the observed [Eu/Fe] abundances have to be searched for. As described in Section 3.1, NSM contribute at a delayed stage to the GCE and in our simulations are unable to reproduce Eu abundances at metallicities [Fe/H] < −2.5. Jet-SNe, however, contribute Eu early, but only in those regions where they occurred, and cause a larger spread in the [Eu/Fe] values (cf.
Section 3.2). We have to test whether it is possible to use the same parameters as in Sections 3.1 and 3.2, since the full combination of both events could lead to an overproduction of elements. We can use the earlier parameter explorations to tune the simulated abundance pattern in order to match the observations. In the following, we will discuss two possible cases.

(i) $P_{\text{NSM}} = 3.4 \times 10^{-4}$, $P_{\text{Jet-SN}} = 0.3$ per cent, $t_{\text{coal}} = 1$ Myr (hereafter model Jet+NSM:A). The results for the model Jet+NSM:A in comparison with observations are shown in Fig. 4. This model provides a reasonable explanation of the observations at lower and higher metallicities, but there is an overproduction of Eu in the range $-2 < [\text{Fe/H}] < -1$. We conclude that larger coalescence time-scales and larger probabilities are necessary regarding NSM, and lower probability of Jet-SNe is necessary to flatten and lower the modelled abundance curve.

(ii) $P_{\text{NSM}} = 3.8 \times 10^{-4}$, $P_{\text{Jet-SN}} = 0.1$ per cent, $t_{\text{coal}} = 10$ Myr (Model Jet+NSM:B). The results for the model Jet+NSM:B in comparison with observations are shown in Fig. 5. This model explains the main features of the abundance curve quite well: the spread at low metallicities, the first confinement of the spread at $[\text{Fe/H}] \approx -2$, the plateau between $[\text{Fe/H}] \approx -2$ and $[\text{Fe/H}] \approx -0.6$, and the second confinement of the spread at $[\text{Fe/H}] \approx -0.2$. However, there still seem to be difficulties at $[\text{Fe/H}] \approx -2$: the scatter in abundances towards low [Fe/H] ratios seems to be a bit too broad. This spread might be slightly reduced by additional mixing terms (e.g. spiral arms mixing) or an additional source providing ratios of [Eu/Fe] = −1, which we did not consider in this work.

Considering Figs 4 and 5, while the results from both models Jet+NSM:A and Jet+NSM:B can reproduce the observed spread of [Eu/Fe] in the early galaxy, model Jet+NSM:B seems to better fit the overall [Eu/Fe] versus [Fe/H] distribution. On the other hand, the evolution of the [Eu/Fe] ratio at low metallicity depends on the r-process production and on the Fe production in CCSNe (see Section 4 and discussion). In Fig. 6, we compare the results for the enrichment history of Eu in the galaxy according to Jet+NSM:A
Figure 6. Enrichment history for models Jet+NSM:A and Jet+NSM:B (cf. Figs 4 and 5 for evolution plots). Magenta stars represent observations, whereas blue dots represent model stars as per Fig. 5 (Model Jet+NSM:B). Red dots representing the enrichment history of the simulation as per Fig. 4 (Model Jet+NSM:A) do not suit the observational data.

and Jet+NSM:B models with observations. While the [Eu/H] versus [Fe/H] ratios predicted by model Jet+NSM:B are in agreement with the observations, model Jet+NSM:A seems to be ruled out.

4 THE IMPORTANCE OF INHOMOGENEITIES

4.1 Inhomogeneities in GCE

From observations of [Eu/Fe] in the early galaxy, one of the main features is a spread in the abundance ratios. Our model is able to reproduce these spreads, mainly because of the inhomogeneous pollution of matter. In Fig. 7, we try to illustrate the effect of applying such an inhomogeneous model. For this purpose, we perform a cut through the xy-plane of the simulation volume for specific time steps. These time steps are marked in the top panel of Fig. 7, in order to provide the reader with a quick glance of the extent of the inhomogeneous element distribution at the correspondent metallicities. For each marker, we provide the complete density field at this specific time step in the middle and lower panels (cf. figure caption for details). We show the extent of inhomogeneities in the middle left-hand panel, for the first marker in the upper panel of the figure. At this time step, we can see – by counting the ‘bubble’-style patterns – that at least three supernovae must have taken place before the snapshot. Since such events give rise to nucleosynthesis, the abundances of metals in such a supernova remnant bubble are higher than outside such a remnant. A star being born inside such a remnant will inherit more metals than a star born outside. Therefore, in the early stages of galactic evolution the stellar abundances are strongly affected by the location where a star is born. Considering much later stages of the evolution, (e.g. the lower right-hand panel of Fig. 7, corresponding to the fourth marker of the upper panel) the supernova remnants have a large overlap. Numerous supernova explosions have contributed lots of nucleosynthesis all over the galaxy. This leads to an averaged distribution of abundances, including different events and an integral over the initial mass function of stars. Therefore, it resembles a ‘mixed’ phase of galactic evolution, where the elements have been homogenized over the whole volume. At this stage of the evolution, it seems not to be so relevant where a star was born. As a consequence, there are smaller differences in the abundance of metals in stars. Therefore, a confinement in the spread of abundances of chemical elements at later stages of the chemical evolution is obtained. Becoming more and more homogeneous, the [Eu/Fe] value converges to a value that can be obtained by integrating the event yields over the whole IMF.

4.2 Instantaneous mixing approximation

A number of recent chemical evolution studies revoked the ‘IMA’ (e.g. Chiappini, Matteucci & Romano 2001; Recchi, Matteucci & D’Ercole 2001; Spitoni et al. 2009). The IMA simplifies a chemical evolution model in terms of mass movement. In detail, all event outputs are expected to mix with the surrounding ISM instantaneously. Such approaches always result in an average value of element ratios for each [Fe/H]. Therefore, in the IMA scheme all stars at a given time inherit the same abundance patterns of elements and it is impossible to reproduce a scatter in the galactic abundances, which seems to be a crucial ingredient at low metallicities. Indeed, instead of a spread of distributions only one value is obtained for
each metallicity. We calculate the best-fitting model (Jet+NSM:B, cf. Fig. 5) with IMA. The result can be found in Fig. 8. The IMA approach may be used to study the chemical evolution trends with a lower computational effort, but Fig. 7 shows that the reproduction of spreads in abundance ratios due to local inhomogeneities requires to use more complex codes as e.g. the ICE code adopted for this work.

While inhomogeneous GCE codes can explain the spread in r-process elements, there is the question whether they might predict a far too large spread for other elements (e.g. α-elements) at low metallicities (with present stellar yields from artificially induced CCSN explosion models). Such effects can also be seen in fig. 1 in van de Voort et al. (2015) for [Mg/Fe], spreading by more than 1 dex, while observations seem to show a smaller spread up to 0.5 dex. This can be related to the amount of supernova ejecta being mixed with the ISM (see discussion above and in Section 5: a more extended mixing reduces this spread), but it can also be related to the supernova nucleosynthesis yields which were never tested before in such inhomogeneous GCE studies. From general considerations of chemical evolution studies, it is found that there are large uncertainties for GCE studies, particularly the influence of stellar yields (e.g. Romano et al. 2010). In Fig. 9, we show the results of model Jet+NSM:B, using the CCSN yields from Nomoto et al. (1997) and Nomoto et al. (2006), which confirms a large spread in [O/Fe], similar to van de Voort et al. (2015) for [Mg/Fe]. However, present supernova yields are the result of artificially induced explosions with constant explosion energies of the order of $10^{51}$ erg. If we consider that explosion energies might increase with the compactness of the stellar core (i.e. progenitor mass; e.g. Perego et al. 2015), the heavier α-elements and Fe might be enhanced as a function of progenitor mass. On the other hand O, Ne, and Mg yields are dominated by hydrostatic burning and also increase with progenitor mass (e.g. Thielemann et al. 1996). This could permit to obtain more constant α/Fe ratios over a wide mass range, although the total amount of ejecta differs (increases) as a function of progenitor mass. This scenario does not take into account all the complexity

**Figure 8.** Same GCE model as in Fig. 5 (Model Jet+NSM:B); however, IMA is applied instead of inhomogeneous evolution. One is able to observe a trend in the abundance evolution, however, the scatter in the abundance pattern is not present anymore (cf. Section 4 for further discussion). The kink at about [Fe/H] = −2.5 is related to the delayed time when NSMs set in and contribute to Eu as well. This figure can also be compared to fig. 2 in Matteucci et al. (2014), which shows the contribution of NSMs alone for various merger delay times and Eu production yields, and fig. 5 in Vangioni et al. (2015) [mergers alone being indicated by black lines]. Thus, also in this approach it is evident that the explanation of [Eu/Fe] at low(est) metallicities by NSM alone is not possible.

and the multidimensional nature of the CCSN event (e.g. Hix et al. 2014, and references therein) that should be considered, but it may be interesting to test its impact in our GCE simulations. In Figs 9 and 10, we show the results for tests where we

(i) replace the Nomoto et al. (1997) iron yields by ad hoc yields, fitting, however, the observed SN 1987A iron production;
(ii) keep the same CCSN rate as in the previous models;
(iii) adopt the parameters to study the r-process nucleosynthesis of Model Jet+NSM:B, obtaining the same [Eu/H] ratio.

This leads, based on the adopted CCSN yields, to a possibility to minimize the spread in α-elements at low metallicities, while
keeping the spread in the r-process element evolution. Therefore, the spread of [O/Fe] obtained from GCE simulations for the early galaxy is strongly affected by the uncertainties in the stellar yields, and it is difficult to disentangle them from more intrinsic GCE uncertainties. This means that at this stage it is not obvious whether an overestimation of the observed [O/Fe] spread is a problem of the ICE code, the observations could rather provide a constraint on stellar yields. In particular, the use of realistic, self-consistent, explosion energies, might reduce the spread at low metallicities to a large extent. Another fundamental point is related to the discussion in Section 3 concerning [Eu/Fe]. At this stage, we consider [Eu/H] as more constraining to study the r-process nucleosynthesis compared to [Eu/Fe], since Fe yields from CCSNe are affected by large uncertainties. Therefore, the model Jet+NSM:B is recommended compared to Jet+NSM:A (see also Fig. 6).

5 CONCLUSION AND DISCUSSION

The main goal of this paper was to reproduce the solar Eu abundance and the evolution of [Eu/Fe] versus [Fe/H] throughout the evolution of the galaxy. For this reason we have studied the influence of two main r-process sites (NSM and Jet-SNe) on the GCE.

Our simulations were based on the ICE model of Argast et al. (2004), with updated nucleosynthesis input for the two sites considered, their respective occurrence frequencies/time delays, and a model resolution of (50 pc)$^3$. The main conclusions are the following.

(i) The production of heavy r-process matter in NSM is evident since many years (see Freiburghaus et al. 1999 and many later investigations up to Korobkin et al. 2012; Bauswein et al. 2013; Rosswog 2013; Rosswog et al. 2014; Wanajo et al. 2014; Eichler et al. 2015; Just et al. 2015; Mendoza et al. 2015). Our implementation of NSM in the ICE model can explain the bulk of Eu (r-process) contributions in the galaxy for [Fe/H] $> -2.5$, but have problems to explain the amount and the spread of [Eu/Fe] at lower metallicities. This is in agreement with the initial findings of Argast et al. (2004). Recent smoothed particle hydrodynamics (SPH)-based studies by van de Voort et al. (2015) make use of a mixing of the ejecta with $3 \times 10^5$ M$_\odot$, a further study by Shen et al. (2015) utilizes a mixing with $2 \times 10^5$ up to $8 \times 10^5$ M$_\odot$. The mixing volume we utilize, based on the Sedov–Taylor blast wave approach, would be related to a subgrid resolution in these studies, but this treatment is essential for the outcome. Mixing initially with a larger amount of matter causes smaller [Fe/H] ratios into which the r-process material is injected.

We have tested such differences in mixing volumes/masses also within our ICE approach. Fig. 11 shows the results we obtain when changing from the Sedov–Taylor blast wave approach to a mixing mass of $2 \times 10^5$ M$_\odot$ (like in Shen et al. 2015), and we can see that we essentially reproduce their results. On the other hand, a higher resolution test in section 3.1 of van de Voort et al. (2015) is essentially in agreement with our results presented above. Thus, these differences are not based on the differences in sophistication of the multidimensional hydrodynamics approach, permitting to model energy feedback from supernovae, outflows, and infall, they can rather be linked directly to the mixing volumes of supernova ejecta. This requires further studies in order to understand whether there exist physical processes (on the time-scale of the delay between the supernova explosions and the merger event) which permit a mixing beyond the Sedov–Taylor blast wave approach.

(ii) The production of heavy r-process elements in a rare species of CCSNe with fast rotation rates and high magnetic fields, causing (fast) jet ejection of neutron-rich matter along the poles has first been postulated by Cameron (2001). This was followed up in rotationally symmetric 2D calculations by Fujimoto et al. (2006, 2008) and the first 3D calculations by Winteler et al. (2012). These calculations still depend on unknown rotation velocities, and magnetic field configurations before collapse, however, they agree with the observations of magnetars and neutron stars with magnetic fields of the order $10^{15}$ G which make up about 1 per cent of all observed neutron stars. Further 3D calculations by Mösta et al. (2014) and recent 2D calculations by Nishimura, Takiwaki & Thielemann (2015) might indicate that not all events leading to such highly magnetized neutron stars are able to eject the heaviest r-process elements in solar proportions. Thus, probably less than 1 per cent of all CCSNe end as Jet-SNe with a full r-process.

When introducing Jet-SNe with ejecta as predicted by Winteler et al. (2012), they can fill in the missing Eu at lower metallicities and reproduce the spread in [Eu/Fe], in agreement with the recent findings of Cescutti & Chiappini (2014). We find that a fraction of 0.1 per cent of all CCSNe which end up in this explosion channel provide the best fit. This would mean that not all but only a fraction of magnetar events which produce the highest magnetic field neutron stars are able to eject a main r-process composition of the heaviest elements, as discussed above.

Our conclusion is that both sites acting in combination provide the best scenario for understanding [Eu/Fe] observations throughout galactic history, with typical probabilities for NSM formations and (merging) delay times as well as probabilities for Jet-SNe. As a side effect we realized that present supernova nucleosynthesis yield predictions, based on induced explosions with a single explosion energy throughout the whole mass range of progenitor stars, bear a number of uncertainties. While apparently too large scatters of $\alpha$/Fe ratios can be obtained in inhomogeneous chemical evolution models, when utilizing existing nucleosynthesis predictions from artificial explosions with energies of 1 Bethe, this might not be due to the chemical evolution model. Such deficiencies can be cured by assuming larger mixing masses with the ISM for supernovae explosions (Shen et al. 2015; van de Voort et al. 2015), or the introduction of an artificial floor of abundances based on IMF-integrated yields.

![Figure 11. Effect of slightly increased sweep-up mass on GCE. Magenta stars represent observations. Red dots show model stars as per our reference model Jet+NSM:B. Blue dots represent a model where every CCSN pollutes $2 \times 10^5$ M$_\odot$ of ISM. The dominant effect of this increased sweep-up mass is to decrease the scatter of abundances and to shift the abundance curve towards lower metallicities.](image-url)
of CCSNe for metallicities at [Fe/H] = −4, but it could in fact just be due the non-existence of self-consistent CCSNe explosion models. We have shown that an explosion energy dependence on the compactness of the Fe core, related to the main-sequence mass, could solve this problem as well by modifying the nucleosynthesis results. Therefore, self-consistent core-collapse calculations with explosion energies varying with progenitor mass and possibly other properties like rotation are highly needed. Although we have obtained a good accordance with the observed Eu abundances, the true origin of r-process elements might still require additional insights. The present investigation may be used to put constraints on the yields, as well as essential properties and occurrence frequencies of sites.

There exist a number of open questions not addressed in the present paper, related (a/b) to production sites and (c) to the true chemical evolution of the galaxy.

(a) As discussed in detail in Section 2.2.2, we did not include ‘regular’ CCSNe from massive stars as contributors to the main or strong r-process, producing the heaviest elements in the Universe. However, as already mentioned in Section 2.2.2, there exists the chance for a weak r-process, producing even Eu in a Honda-style pattern in such events. This could provide the correct lower bound of [Eu/Fe] in Fig. 5 and would be consistent with the recent findings of Tsujimoto & Shigeyama (2014).

(b) We did not include the effect of NS–BH mergers in the present paper. They would result in similar ejecta as NS–NS mergers per event (Korobkin et al. 2012), but their occurrence frequencies bear high uncertainties (Postnov & Yungelson 2014). Mennekens & Vanbeveren (2014) provide a detailed account of their possible contribution and also discuss their contribution to global r-process nucleosynthesis. One major difference with respect to our treatment of NSM in chemical evolution relates to the fact that (if the black hole formation is not causing a hypernova event but rather occurring without nucleosynthesis ejecta) only one CCSN is polluting the ISM with Fe before the merger event, in comparison to two CCSNe. This would lead to a smaller [Fe/H] ratio in the ISM which experiences the r-process injection, and just to an ‘earlier’ appearance of high [Eu/Fe] ratios in galactic evolution. If we assume that BH formations are as frequent as supernova explosions, an upper limit of the effect would be that all NS–NS mergers are replaced by BH–NS mergers, moving the [Eu/Fe] features to lower metallicities by a factor of 2. However, the lower main-sequence mass limit for BH formation is probably of the order 20 M⊙, and only a small fraction of core collapses end in black holes. Therefore, we do not expect that the inclusion of NS–BH mergers shifts the entries by more than 0.15 in Fig. 1. This by itself would not be a solution in terms of making only compact (i.e. NS–NS and NS–BH) mergers responsible for the r-process at very low metallicities.

(c) There have been suggestions that the Milky Way in its present form resulted from merging subsystems with a different distribution of masses. Such ‘dwarf galaxies’ will experience different star formation rates. It is known that different star formation rates can shift the relation [X/Fe] as a function of [Fe/H]. If the merging of such subsystems will be completed at the time when Type Ia supernovae start to be important, the relation [X/Fe] = f([Fe/H]) will be uniform at and beyond [Fe/H] > −1, but it can be blurred for low metallicities between the different systems, possibly leading also to a spread of the onset of high [Eu/Fe] ratios at low metallicities (Ishimaru et al. 2015). The result depends on the treatment of outflows, should in principle be tested in inhomogeneous models, and also already be present in the simulations of van de Voort et al. (2015) and Shen et al. (2015). But it surely requires further investigations to test fully the impact of NSM on the r-process production in the early galaxy.

Future studies will probably require a distribution of delay times for NSM events, a test of the possible contributions by BH–NS mergers, a better understanding of yields, and improvements in understanding mixing processes after supernovae explosions and during galactic evolution. Testing the full set of element abundances from SNe Ia and CCSNe as well as the two sources discussed above, in combination with extended observational data, will provide further clues to understanding the evolution of galaxies.

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