Optimal Operating Scenario for Polerood Hydropower Station to Maximize Peak Shaving and Produced Profit

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ABSTRACT. This paper deals with the optimization of the daily operation of Polerood hydropower station being constructed in the north of Iran. Dynamic Programming method (DP) is applied as the preferred optimization tool owing to the fact that it guarantees the optimal solution and is applicable to the present problem. Produced profit and peak-shaving are the two objectives considered separately in this study. The results show that the optimal water management of the case study through charging and discharging the reservoir at the appropriate times led to 4% increase in the produced profit. In another part of this study, the optimal performance strategies regarding to the two objectives (produced profit and peak-shaving) are compared. The observed similarity between the two performance strategies implies the substantial dependence of the electricity price and the network demand level. The paper ends with the profitability study of the project and the sensitivity analysis of the results to various economic parameters.

Keywords: Polerood Hydropower Station; Performance Optimization; Dynamic Programming Method; Profit; Peak Shaving

1. Introduction

Global energy demand has grown from 6630 million tons of oil (MTO) in 1980 to 11295 MTO in 2008 with the rate of 5.4% per year (Darmstader, Teitelbaum, & Polach 1971, Martinot 2005, Finley 2013). The crude oil and natural gas resources will be depleted in the coming decades (Barten 2010). Furthermore, the greenhouse gases being generated from the fossil fuels have serious effects on human’s lives (Hosseini & Wahid 2013).

Using the renewable sources of energy is the most valuable approach to overcome the previously mentioned problems (Nautiyal, Singal, & Sharma 2011). Among the renewable forms of energy, hydroelectric energy with the approximate production cost of 0.04 $/kWh seems to be more economical (Delucchi & Jacobson 2011). Moreover, the hydroelectric systems are easy from the maintenance standpoint based on their simple design, and the energy generated by these systems is more reliable in comparison to the other renewable systems (Egré & Milewski 2002, Gaudard & Romero 2014).

Traditional patterns of water management cannot cope with today’s needs including various objectives and constraints; accordingly, the optimal management of hydropower systems seems to be necessary (Labadie 2004, Lu et al. 2013).

Various research works have been performed concerning the performance optimization of the

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respectively. A new method named “Self-Learning Genetic Algorithm (GA)” was proposed by Hakimi-Asiabar, Ghodsypour, & Kerachian (2010) to optimize the operation of “Dez” HPS in Iran. The results showed improvements in the objective value and convergence speed in comparison to the previous version called “Som-Based Multi-objective Genetic Algorithm”. Pérez-Díaz & Wilhelmi (2010) applied “Mixed Integer Linear Programming (MILP)” to maximize the produced profit of a real HPS. Some environmental constraints such as a limitation for the rate of change of discharged flow were considered in this study. Multi-objective performance optimization of a hydropower station, with the aim of maximizing power generation and minimizing the difference between the power production and demand, was addressed by Afshar (2012). In this study, “Partially Constrained Particle Swarm Optimization (PSO)” and “Fully Constrained PSO” methods were employed, and the better results with lower computation times were achieved in comparison to the simple PSO and GA. Chen et al. (2013) employed GA to maximize the power generation of a HPS with some environmental constraints. The results showed that 50-70% of the fishes survived at the expense of 3.6-6% reduction in the generated energy.

Multi-objective optimization of eight cascaded reservoirs by using a hybrid global optimization algorithm was addressed by Jiekang, Zhuanzhi, & Fan (2014). Maximization of the generated power and maximization of the volume of water stored behind the reservoirs constituted the objectives of this study. Xu & Tao (2012) used “Brindom Simulation based GA” for multi-objective optimization of a HPS. Appropriate water allocation to different consumers (e.g., irrigation, and residential and industrial users), as well as the maximum balance between the power production and demand constituted the objectives of this work. The selected method was evaluated through comparing the results to those obtained from “Fuzzy Programming” and “Stochastic” methods.

Optimization tools have been used by Jahanideh-Tehrani, Bozorg Haddad, & Loàiiciga (2015) to overcome climate changes. They showed that higher energy production can be obtained by applying optimization tools. Based on different inflow rates and electricity prices, Mahmoudimehr, Sorouri, & Feshalami (2016) presented a novel map in order to choose the best type of a hydropower plant from economical factors points of view. The uncertainty in future prices and inflow on stochastic short-term hydropower scheduling has also been investigated by Belsnes et al. (2016). Gaudard, Avanzi, & De Michele (2017) weighed the effects of price seasonality variation on revenue against climate change and concluded that price seasonality causes more uncertainty on revenue than climate change.

There also exist some other research works (Chatterjee, Howitt, & Sexton 1998, Mantawy, Soliman, &El-Hawary 2003, Chen, McPhee, &Yeh 2007, Sharma, Jha, &Naresh 2007, Borghetti et al. 2008, Yoo 2009, Amjady & Soleymanpour 2010, Fu et al. 2011, Ma, Lian, &Wang 2013, Zhang et al. 2013, Yang et al. 2015, Bozorg-Haddad et al. 2017) which have employed different optimization methods, including Tabu Search, Neural Network, GA, MILP, LP, DE, PSO, symbiotic organisms search, and MOSPD to optimize the operation of a hydropower station. The produced profit, generated power, production duration, operating costs, and the difference between power production and demand, constitute the various objectives which considered in these works.

Optimization approaches can be classified into a number of primary groups, including the mathematical (derivative-based and derivative free), heuristic (unproven and originated from the past experiences), and evolutionary (such as GA) algorithms (Koziel & Yang 2011). On condition that DP, as a derivative-free mathematical method, is applicable to a problem, it guarantees the global optimal solution, whereas the other previously mentioned methods do not and may be trapped in a local optimum solution (Pérez-Díaz & Wilhelmi 2010, Afshar 2012, Chen et al. 2013). A local optimum is a selection which is only better than the neighbouring selections. By contrast, a global optimum is a selection from a given domain which is better than any other selection in that domain.

The main objective of this paper is to apply DP to optimize the daily operation of Polerood HPS being constructed in the north of Iran. Furthermore, the optimization procedure is executed for two different objectives (i.e., the produced profit and peak shaving). The optimal operating strategies related to the two considered objectives are compared and analysed. Additionally, the profitability of the project is investigated and its sensitivity to various parameters is reported.

2. Problem definition

Fig. 1 shows a schematic view of the hydropower system considered in this study.

Eqs. (1)-(7) show the objective functions and constraints of the problem which are explained in the following.

Maximize \[
\sum_{i=1}^{T} P_{o,i} \cdot Price
\]  
(1)  

Minimize \[
\sum_{i=1}^{T} (P_{Gi} - P_{sh,i})^2
\]  
(2)  

\[
\begin{align*}
\text{if } P_{demand,i} \geq P_{capacity} \rightarrow P_{sh,i} &= P_{demand,i} - P_{capacity} \\
\text{else} \rightarrow P_{sh,i} &= 0
\end{align*}
\]  

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\[ P_{G,i} = \alpha Q_{d,i} \eta \]  

(3)

\[ v_i = v_{i-1} + \left( Q_{d,i-1} - Q_{d,i} \right) \Delta t \]  

(4)

\[ v_{\min} < v_i < v_{\max} \]  

(5)

\[ 0 \leq Q_{d,i} \leq Q_{d,\max} \]  

(6)

\[ u_T \geq u_0 \]  

(7)

Eq. (1) defines the total produced profit as the first objective function. In Eq. (1), \( P_{G,i} \) and \( Price \) represent the generated power (W) and electricity price ($/kWh), respectively, at time interval i. In this study, the operation is optimized over a period of one day, and the whole period was divided into 24 one-hour intervals. Also, \( T \) represents the time period (h).

Eq. (2) defines the peak shaving as the second objective function. In Eq. (2), \( P_{sh} \) denotes the power shortage (W) which is defined as the difference between the network capacity (i.e., the maximum power that can be supplied to the network) and power demand when the latter exceeds. \( P_{demand} \) and \( P_{capacity} \) are Network capacity (W) and Electrical power demand (W), respectively.

Eq. (3) shows the generated power as a function of discharged flow rate through the turbines \( (Q d \text{ (m}^3\text{/s}) \). In this equation \( \eta \) denotes mechanical to electrical energy conversion efficiency, and \( \alpha \) is a head dependent parameter which is considered as a constant coefficient in this study.

Eq. (4) shows the reservoir’s mass balance. In this equation \( Q_{sh} \) and \( v \) designate the reservoir’s inflow rate \( (\text{m}^3\text{/s}) \) and the volume \( (\text{m}^3) \) of water behind the reservoir, respectively. \( v_{\min} \) and \( v_{\max} \) are the minimum and maximum volumes of the water behind the dam, respectively. Eq. (5) specifies a permissible range for the volume of water behind the reservoir. Eq. (6) shows the maximum allowable rate of flow passing through the turbines.

Based on the constraint shown in Eq. (7), the final volume of water behind the reservoir \( (v_T) \) must be greater than or equal to its initial value \( (v_0) \).

3. Dynamic Programming Algorithm and Verification of the Developed Program

DP method was invented by an American mathematician named Bellman (Bellman 2013). This method has been described in some references (Carter, 2012; Mahmoudimehr, Marano, Rizzo, & Tiano 2012; Mahmoudimehr, Sorouri, & Feshalami 2016). This section explains how DP is applied to the problem under study. For each time interval, the volume of water behind the reservoir is considered to be the decision variable. Consequently, \( [v_1, v_2, ..., v_T] \) is the set of decision variables of the problem. At first, the continuous range of each decision variable (i.e., the domain with the lower and upper bounds of \( v_{\min} \) and \( v_{\max} \)) must be discretized into a set of discrete values \( \{v_{\min}, v_{\min} + \Delta v, v_{\min} + 2\Delta v, ..., v_{\max}\} \), where \( \Delta v \) denotes the step size of discretization. Accordingly, the optimal value of each decision variable is to be selected from the set of discrete values instead of the continuous range. If \( \Delta v \) is sufficiently small, the solution will be sufficiently close to the global optimum.

The DP procedure is the same for the two objectives; therefore, the DP method is only explained for the first objective (i.e., maximization of produced profit). The DP procedure is mathematically shown in Eq. (8). It is worth noting that the initial water head \( (v_0) \) is considered to be a known value. The revenue in a time interval, \( Objective \), can be considered as a function of only the heads of water at the beginning and at the end of that time interval (i.e., \( v_{i-1} \) and \( v_i \), respectively).

As shown in Eq. (8), in the first step of the DP procedure, only the first two time intervals are considered. The total revenue from the beginning to the end of time interval 2 is the sum of the revenues in time interval 1 \( (Objective(v_{i-1}, v_i)) \) and time interval 2 \( (Objective(v_{i-1}, v_i)) \). In this step, as shown in Eq. (8), for each discrete value of \( v_2 \), the maximum possible revenue from the beginning to the end of time interval 2 (denoted by \( Objective(v_{i-1}, v_2) \)) is found through examining all discrete values of \( v_1 \). After this step, \( v_1 \) is no longer an independent decision variable because for each value of \( v_2 \) the best value of \( v_1 \) has been determined. Therefore, \( v_1 \) can be removed from the decision vector. Assuming that the continuous range of each decision variable is discretized into \( N \) discrete values, the order of computational complexity of the first step is \( N^2 \).

First step: \[ Objective_{i-1}(v_i) = \max_{v_1} \{Objective_{i-1}(v_{i-1}, v_1) + Objective_{i-1}(v_1, v_i)\} \]

second step: \[ Objective_{i-1}(v_i) = \max_{v_1} \{Objective_{i-2}(v_{i-1}, v_1) + Objective_{i-1}(v_1, v_i)\} \]

Last step: \[ Objective_{i-1}(v_i) = \max_{v_1} \{Objective_{i-2}(v_{i-1}, v_1) + Objective_{i-1}(v_1, v_i)\} \]

In the second step, one more time interval is considered. In this step, as shown in Eq. (8), for each discrete value of \( v_2 \), the maximum possible revenue from the beginning to the end of time interval 3 (denoted by \( Objective_{i-2}(v_2) \)) is determined through examining all discrete values of \( v_2 \). It is worth mentioning that \( Objective_{i-2}(v_2) \) has been computed in the previous step and does not need to be computed again. Moreover, \( v_2 \) is no longer an independent decision variable and can be removed from the decision vector. Similar to the first step, the order of computational complexity of this step is \( N^2 \).

The procedure continues until the maximum revenue from the beginning to the end of time interval 24 (denoted by \( Objective_{24}(v_{23}) \)) is obtained as a function of only \( v_{24} \), hence, the maximum daily revenue can be obtained through examining all values of \( v_{24} \).

Since for each value of \( v_3 \), the optimal value of \( v_{24} \) has been determined during the DP steps, after the optimal value of \( v_{24} \) is found, the optimal values of \( v_{23} \) to \( v_1 \) can be obtained one by one through a back-tracking process. Based on the previously described procedure, the DP method reduces the order of computational complexity from \( N^{24} \) (because there are 24 decision variables and each decision variable can take \( N \) discrete values) to \( 24N^2 \).
DP method guarantees the optimal solution based on its mathematical logic which has been described. However, to verify the optimization computer code developed by these authors, it is applied to a problem defined in Zhao & Davidson (2009) study and the results are compared to those of (Zhao & Davison 2009) which were also obtained by DP method.

The specifications of the verification case study are as follows: The operating period of 48 hours, the natural inflow rate of $3\pi (m^3/s)$, the initial head of 120 m, the minimum and maximum allowable heads of 120m and 180 m, respectively, a cubic reservoir with the surface area of 3600 m$^2$, and the constant electricity price of 1 $$/MWh.

Fig. 2 shows a comparison of the optimal time variation of the water head behind the reservoir obtained in the present work to that reported by Zhao & Davidson (2009). As is observed, the results are acceptably matched with the negligible maximum difference of about 0.2%.

![Fig. 2. Comparison of the optimal time variation of water head in the present work and that of Zhao & Davison (2009)](image)

4. Case study: Polerood hydro power station

“Polerood” HPS is under construction on “Polerood” river in Guilan province located in the north of Iran. The installed capacity will be 16.6 MW (composed of two 8.3-MW units). For this case, $Q_{lim}$, $Q_{lin}$, $\alpha$ and $\eta$, were considered to be 20, 8, $10^6$, and 0.83, respectively.

![Fig. 3. Electricity price scenario](image)

Fig. 3 illustrates the electricity price scenario needed for the first objective function (the produced profit). Fig. 4 shows the network capacity as well as the hourly data of Iran's electrical power demand. The red filled bars in this figure indicate the times at which the demands are greater than the network capacity (or there exist power shortages). It is worth mentioning that the value of inflow rate and the data in Figs. 3 and 4 are related to a representative summer day.

![Fig. 4. Iran's electrical power demand](image)

![Fig. 5. Optimal time variation of the volume of water behind the reservoir](image)

5. Results and discussion

The results of the first and second objective functions as well as their comparison, and the profitability study of the project are presented in this section.
5.1. Profit maximization

Fig. 5 illustrates the optimal set of decision variables ([n₁, n₂,..., nₙₙ]). Furthermore, the optimal hourly variation of the generated power, related to the optimal solution, along with the electricity price scenario, is shown in Fig. 6. Fig. 6 illustrates how the generated power follows the electricity price scenario to achieve the maximum total profit.

As shown in Fig. 5, the water is stored behind the reservoir at the times with low electricity prices, and the stored water is discharged to produce maximum electricity during periods of high electricity prices. To estimate the benefit of using the optimization procedure for determining the performance strategy, the optimal objective value (i.e., $16532$) is compared to that obtained by assuming that the volume of water behind the reservoir does not change with time. This assumption, which implies that the discharged flow through the turbines equals the inflow Qᵢᵩᵢ = Qᵢᵩᵢ at all times, yielded the objective value of $15936$ which was about 4% lower than that obtained through optimization process.

5.2. Peak shaving

Fig. 7 shows optimal time variation of generated power along with the time variation of the power shortage. This figure indicates how the generated electrical power follows the power shortage. As shown, the electricity generation is zero for initial times of operation because as mentioned before, the contents of network capacity are higher than that of demand. However, by reaching to the peak time of consumption, this point is reversed. Therefore, the power plant begins to produce power in order to compensate the lack of demand power. Additionally, this figure shows trueness of the algorithm applied in this research. Consequently, it can be claimed that this scenario is the optimal condition to shave peak load presented in this research.

5.3. Comparing the results of the two objective functions

Fig. 8 compares the optimal performance curves obtained for the two different objective functions (i.e., profit and peak shaving). The similarity between the performance strategies implies that the electricity price is significantly related to the demand level. This could also be perceived through comparing Figs. 3 and 4 where the price has the same trend as the power demand. However, the observed discrepancies in Fig. 8, shows a need for modifying the price scenario.

Table 1

| C₁ (M$) | n (year) | m | I | Annually averaged inflow rate (m³/s) |
|---------|----------|---|---|----------------------------------|
| 70      | 70       | 0.02 | 0.05 | 15                               |

5.4. Profitability Study and Sensitivity Analysis

This section is concerned with investigating the economic feasibility of the project and the sensitivity of the results to the various parameters.

In this work, Net Present Value (NPV) is considered as the criterion for the feasibility study. NPV, which is expressed in Eq. (9), is defined as the net value of all benefits and costs of the project, discounted back to the beginning of the investment. If the NPV is greater than zero, the project is considered to be economically acceptable as it will bring profit to the investor. In Eq. (9), B₁ denotes annual revenue from electricity sales, I shows interest rate, n represents the lifetime of the system, and C₁ is the initial investment cost. Moreover, the annual operating and maintenance cost is considered to be a fraction (m) of the initial investment cost.

\[
\text{NPV} = B₁ \left[ \frac{(1 + I)^{-n} - 1}{I(1 + I)} \right] - C₁ \left[ 1 + m \left( \frac{(1 + I)^{-1} - 1}{I(1 + I)} \right) \right] \tag{9}
\]

The economic specifications of the project together with the annually averaged inflow rate are gathered in Table 1. The electricity price scenario has been previously shown in Fig. 3, and B₁ (annual revenue) is obtained through optimization procedure which has been previously discussed. Calculations, based on the information presented in Table 1, resulted in the approximate annual revenue and NPV of $11.1 M$ and $117.6 M$, respectively. The positive value of NPV indicates that the project is economically feasible. However, regarding to the fact that the parameters of Table 1 have the uncertain nature, the sensitivity of the results to these parameters is studied and illustrated in Fig. 9.
Fig. 9a illustrates the sensitivity of NPV and Bₐ to the inflow rate. This figure indicates that both NPV and Bₐ increase with inflow rate. Moreover, the project is economically feasible (i.e., takes positive value of NPV) for the considered range of inflow rate (10 to 19 m³/s).

The electricity price scenario previously shown in Fig. 3 with the average value of 100 $/MWh was considered as the base price scenario. To study the effect of electricity price on the feasibility of the project, calculations were carried out for the different average values of electricity price (from 20 $/MWh to 120 $/MWH), and the results are shown in Fig. 9b. As is observed, both NPV and Bₐ increase with the electricity price. Moreover, the results show that the project becomes unprofitable for the average electricity price below 40 $/MWh. The effects of interest rate, and the lifetime of project, on NPV are shown in Figs. 9c and 9d, respectively. It is observed that NPV increases with lifetime, but decreases with interest rate. Fig. 9d indicates that the project is profitable (with positive values of NPV) for the considered lifetime (30-90 years). However, Fig. 9c shows that the project is acceptable up to an interest rate of 14 per cent.

6. Conclusion

Dynamic programming method guarantees the optimal solution and therefore is of great importance. The present study describes how to use dynamic programming method to optimize the daily operation of a hydropower station.

Then, the DP method was applied to “Polerood” dam which is being constructed in the north of Iran. The results were obtained for the two different objective functions (profit and peak-shaving). It was observed that the optimization process could improve the results. Comparison of the results of the two objectives confirms the fact that electricity price is mainly a function of demand level. However, the observed discrepancy shows that the price scenario should be updated as the network capacity and/or the power demands change. Finally, it was shown that the project is profitable based on the net present value (NPV) criterion, and the sensitivity of the economic feasibility of the project to various economic parameters was investigated.

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