Channel Assignment for Throughput Maximization in Cognitive Radio Networks

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Abstract—In this paper, we consider the channel allocation problem for throughput maximization in cognitive radio networks with hardware-constrained secondary users. Specifically, we assume that secondary users exploit spectrum holes on a set of channels where each secondary user can use at most one available channel for communication. We develop two channel assignment algorithms that can efficiently utilize spectrum opportunities on these channels. In the first algorithm, secondary users are assigned distinct sets of channels. We show that this algorithm achieves the maximum throughput limit if the number of channels is sufficiently large. In addition, we propose an overlapped channel assignment algorithm, that can improve the throughput performance compared to the non-overlapped channel assignment algorithm. In addition, we design a distributed MAC protocol for access contention resolution and integrate the derived MAC protocol overhead into the second channel assignment algorithm. Finally, numerical results are presented to validate the theoretical results and illustrate the performance gain due to the overlapped channel assignment algorithm.

Index Terms—Channel assignment, MAC protocol, spectrum sensing, throughput maximization, cognitive radio.

I. INTRODUCTION

Emerging broadband wireless applications have been demanding unprecedented increase in radio spectrum resources. As a result, we have been facing a serious spectrum shortage problem. However, several recent measurements reveal very low spectrum utilization in most useful frequency bands [1]. Cognitive radio technology is a promising technology that can fundamentally improve the spectrum utilization of licensed frequency bands through secondary spectrum access. However, transmissions from primary users should be satisfactorily protected from secondary spectrum access due to their strictly higher access priority. Protection of primary communications can be achieved through interference avoidance or interference control approach (i.e., spectrum overlay or spectrum underlay) [1].

For the interference control approach, transmission powers of secondary users should be carefully controlled so that the aggregated interference they create at primary receivers does not severely affect ongoing primary communications [2]. In most practical scenarios where direct coordination between primary and secondary users is not possible and/or when distributed communications strategies are desired, it would be very difficult to maintain these interference constraints. The interference avoidance approach instead protects primary transmissions by requesting secondary users to perform spectrum sensing to discover spectrum holes over which they can transmit data. Developing efficient spectrum sensing and access mechanisms have been very active research topics in the last several years [3]–[13]. This paper focuses on developing efficient channel assignment algorithms for spectrum sharing in a cognitive radio network with hardware-constrained secondary nodes.

In particular, we consider the scenario where each secondary user can exploit only one available channel for communications. This can be the case where secondary users’ transceivers are equipped with only one radio with a narrow-band RF front end [14]. In addition, it is assumed that white spaces are so dynamic that it is not affordable for each secondary user to sense all channels to discover available ones and/or to exchange sensing results with one another. Under this setting, we are interested in determining a set of channels allocated for each secondary user in advance so that maximum network throughput can be achieved in a distributed manner. To the best of our knowledge, this important problem has not been considered before.

Because the underlying problem is NP-hard, we develop two greedy non-overlapped and overlapped channel assignment algorithms, which can work very efficiently. In addition, we design and analyze a distributed MAC protocol which is integrated into the overlapped channel assignment algorithm. We demonstrate through numerical studies that if the number of channels is large then the proposed non-overlapped channel assignment works efficiently. In addition, the overlapped channel assignment algorithm can achieve noticeable network throughput improvement compared to the non-overlapped counterpart if the number of channels is small or moderate.

The remaining of this paper is organized as follows. Section II describes the system model and problem formulation. We present a non-overlapped channel assignment algorithm and describe its performance in Section III. Development of overlapped channel assignment and the corresponding MAC protocol is considered in Section IV. Section V demonstrates numerical results followed by concluding remarks in Section VI.

II. SYSTEM MODEL AND PROBLEM FORMULATION

A. System Model

We consider the collocated cognitive radio network in which $M$ secondary users exploit spectrum opportunities in $N$ channels. We assume that each secondary user can use at most one channel for his/her data transmission. In addition, time is divided fixed-size cycle where secondary users perform sensing on assigned channels at the beginning of each cycle to explore available channels for communications. We assume that sensing time is negligible compared to the cycle time and there is no sensing error. It is assumed that secondary users transmit at a constant rate which is normalized to 1 for throughput calculation purposes.
We consider two different channel assignment schemes. In the first scheme, secondary users are assigned distinct sets of channels. This channel assignment scheme simplifies the spectrum sharing design because secondary users do not compete for the same available channels. However, it overlooks the potential diversity gain of the spectrum sharing problem. In the second scheme, we allow secondary users to sense and operate on overlapped channels. When one particular channel is exploited by several secondary users, it is assumed that a Medium Access Control (MAC) protocol is employed to resolve the channel contention.

B. Problem Formulation

We are interested in performing channel assignment to maximize the system throughput. Let $T_i$ denote the throughput achieved by secondary user $i$. Let $x_{ij}$ describe the channel assignment decision where $x_{ij} = 1$ if channel $j$ is assigned to secondary user $i$ and $x_{ij} = 0$, otherwise. Then, the throughput maximization problem can be formally written as follows:

$$\max \sum_{i=1}^{M} T_i. \quad (1)$$

For non-overlapped channel assignments, we have following constraints

$$\sum_{i=1}^{M} x_{ij} = 1, \quad \text{for all } j. \quad (2)$$

We can derive the throughput achieved by secondary user $i$ for non-overlapped channel assignment as follows. Let $S_i$ be the set of channels assigned to secondary user $i$. Let $p_{ij}$ be the probability that channel $j$ is available at secondary user $i$. For simplicity, we assume that $p_{ij}$ are independent from one another. This assumption holds when each secondary user impact different set of primary users on each channel. This can indeed be the case because spectrum holes depend on space. Note, however, that this assumption can be relaxed if the dependence structure of these probabilities is available. Under this assumption, $T_i$ can be calculated as

$$T_i = 1 - \prod_{j \in S_i} p_{ij} = 1 - \prod_{j=1}^{N} \left(1 - p_{ij}\right)^{x_{ij}} \quad (3)$$

where $\overline{p}_{ij} = 1 - p_{ij}$ is the probability that channel $j$ is not available for secondary user $i$. In fact, $1 - \prod_{j \in S_i} \overline{p}_{ij}$ is the probability that there is at least one channel available for secondary user $i$. Because each secondary user can use at most one available channel, its maximum throughput is 1. In the overlapped channel assignment scheme, constraints in (2) are not needed. From this calculation, it can be observed that the optimization problem (1-2) is a non-linear integer program, which is a NP-hard problem. Given the large computational complexity required the considered problem, we will develop sub-optimal and low-complexity channel assignment algorithms in the following.

III. NON-OVERLAPPED CHANNEL ASSIGNMENT

Algorithm

We develop a low-complexity algorithm for non-overlapped channel assignment in this section. Recall that $S_i$ is the set of channels assigned for secondary user $i$. In the non-overlapped channel assignment scheme, we have $S_i \cap S_j = \emptyset$, $i \neq j$. The greedy channel assignment algorithm iteratively allocates channels to secondary users that achieves maximum increase in the throughput. Detailed description of the proposed algorithm is presented in Algorithm 1. In each channel allocation iteration, each secondary user $i$ calculates its increase in throughput if the best available channel (i.e., channel $j^* = \arg \max_{j \in S_i} p_{ij}$) is allocated. This increase in throughput can be calculated as follows:

$$\Delta T_i = T_i^a - T_i^b = \left[1 - \left(1 - p_{ij^*}\right) \prod_{j \in S_i} (1 - p_{ij})\right] - \left[1 - \prod_{j \in S_i} (1 - p_{ij})\right] = p_{ij^*} \prod_{j \in S_i} (1 - p_{ij}). \quad (4)$$

It can be observed from (4) that $\Delta T_i$ will quickly decrease over allocation iterations because $\prod_{j \in S_i} (1 - p_{ij})$ tends to zero as the set $S_i$ is expanded. We have the following property for the resulting channel assignment due to Algorithm 1.

Algorithm 1 NON-OVERLAPPED CHANNEL ASSIGNMENT

1: Initialize the set of available channels $S_a := \{1, 2, \ldots, N\}$ and $S_i := \emptyset$ for $i = 1, 2, \ldots, M$
2: for $i = 1$ to $M$ do
3: $j_i^* = \arg \max_{j \in S_i} p_{ij}$
4: if $S_i \neq \emptyset$ then
5: Find $\Delta T_i = T_i^a - T_i^b$, where $T_i^a$ and $T_i^b$ is the throughputs after and before assigning channel $j_i^*$.
6: else
7: Find $\Delta T_i = p_{ij_i^*}$.
8: end if
9: end for
10: $i^* = \arg \max_i \Delta T_i$.
11: Assign channel $j_i^*$ to user $i^*$.
12: Update $S_a = S_a \setminus j_i^*$.
13: if $S_a$ is empty, terminate the algorithm. Otherwise, return to step 2.

Proposition 1: If we have $N \gg M$, then the throughput achieved by any secondary user $i$ due to Algorithm 1 is very close to the maximum value of 1.

Proof: This proposition can be proved by showing that if the number of channels is much larger than the number of secondary users (i.e., $N \gg M$) then each secondary user will be assigned a large number of channels. Recall that Algorithm 1 assigns channels to a particular secondary user $i$ based on the increase-in-throughput metric $\Delta T_i$. This property can be proved by observing that if a particular secondary user $i$ has been assigned a large number of channels, its $\Delta T_i$ is very close to zero. Therefore, other secondary users who have been
assigned a small number of channels will have a good chance to receive more channels. As a result, all secondary users are assigned a large number of channels if \( N >> M \). According to (3), throughput achieved by secondary user \( i \) will reach its maximum value of 1 if its number of assigned channels is sufficiently large. Hence, we have proved the proposition.

In practice, we do not need a very large number of channels to achieve close-to-maximum throughput. In particular, if each channel is available for secondary spectrum access with probability at least 0.8 then the throughput achieved by a secondary user assigned three channels is not smaller than \( 1 - (1 - 0.8)^3 = 0.992 \), which is less than 1% below the maximum throughput. When the number of channel is not sufficiently large, we can potentially improve the system throughput by allowing overlapped channel assignment. We develop overlapped channel assignment in the next section. After assigning channels using Algorithm 1, i.e., a separate set at each secondary user is established, we calculate throughput of each secondary user by using (3). Then, the total throughput of the whole system can be calculated by summing throughput of all secondary users.

**IV. OVERLAPPED CHANNEL ASSIGNMENT**

Overlapped channel assignment can improve the network throughput by exploiting the multiuser diversity gain. In particular, a channel assigned to only one secondary user cannot be exploited if it is being used by a nearby primary user. However, if a particular channel is assigned to several secondary users then it is more likely that it can be exploited by at least one secondary user. However, when several secondary users attempt to access the same assigned channel, a MAC protocol is needed to resolve the access contention. This MAC protocol incurs overhead that offsets the throughput gain due to the multiuser diversity. Hence, sophisticated channel assignment algorithm is needed to balance the protocol overhead and throughput gain.

**A. MAC Protocol**

Let \( S_i \) be the separate set of channels assigned for secondary user \( i \) and \( S_i^{\text{com}} \) be the set of channels assigned for both users \( i \) and other users. Let denote \( S_i^{\text{tot}} = S_i \cup S_i^{\text{com}} \), which is the set of all channels assigned to user \( i \). Assume that there is a control channel, which is always available and used for contention resolution of channel access. We consider the following MAC protocol run by any particular secondary user \( i \), which belongs the class of synchronized MAC protocol [15]. After sensing assigned channels, each user \( i \) proceeds as follows. If there is at least one channel in \( S_i \) available, then user \( i \) chooses one of these available channels randomly for communication. If this is not the case, user \( i \) will choose one available channel in \( S_i^{\text{com}} \) randomly (if there is any channel in this set available) (for brevity we simply call users instead of secondary users when there is no confusion). Then, it chooses a random backoff value which is uniformly distributed in the interval \([0, W-1]\) (i.e., \( W \) is the contention window) and starts.
decreasing its backoff counter while listening on the control
channel.

If it overhears transmissions of RTS/CTS from any other
users, it will freeze from decreasing its backoff counter until
the control channel is free again. As soon as a user’s backoff
counter reaches zero, its transmitter transmits an RTS message
containing a chosen channel to its receiver. If the receiver
successfully receives the RTS, it will reply with CTS and
user \( i \) starts its communication on the chosen channel for the
remaining of the cycle. In addition, by overhearing RTS/CTS
messages of neighboring users, which convey information
about the channels chosen for communications, other users
compared these channels with their chosen ones. Any user
who has his/her chosen channel coincides with the overheard
channels quits the contention and waits until the next cycle.
Otherwise, it will continue to decrease its backoff counter
before exchanging RTS/CTS messages. The MAC protocol is
illustrated in Fig. 1 where sensing and synchronization phases
are employed before the channel contention and transmission
phase in each cycle. Note that the fundamental aspect that
makes this MAC protocol different from that proposed in
[6] is that in [6] we assumed each winning user can use all available channels for communications while at most one
available channel can be exploited by hardware-constrained
secondary users in this current paper. Therefore, the channel
assignment problem does not exist for the setting considered
in [6].

B. Channel Assignment Algorithm

We develop an overlapped channel assignment algorithm
as follows. First, we run Algorithm 1 to obtain the non-
overlapped channel assignment solution. Then, we start per-
foming overlapped channel assignment by allocating channels
that have been assigned to a particular user to other users.
The MAC protocol overhead typically increases when a larger
number of secondary users compete for the same channel.
Therefore, to achieve the optimal tradeoff between overhead
and the multiuser diversity gain, only small number of users
should share any channel.

We devise a greedy overlapped channel assignment algo-
rum using the increase-of-throughput metric similar to that
employed in Algorithm 1. However, calculation of this metric
exactly turns out to be a complicated task. Hence, we employ
an estimate of the increase-of-throughput, which is derived in
the following to perform channel assignment assuming that
the MAC protocol overhead is \( \delta < 1 \). In fact, \( \delta \) depends on
the outcome of the channel assignment algorithm (i.e., sets of
channels assigned to different users). Therefore, we will show
how to calculate \( \delta \) and integrate it into this channel assignment
algorithm later.

Consider a case where channel \( j \) is the common channel
of users \( i_1, i_2, \ldots, i_{MS} \). Here, \( MS \) is the number of users
sharing this channel. We are interested in estimating the
increase in throughput for a particular user \( i \) if channel \( j \)
is assigned to this user. Indeed, this increase of throughput can
be achieved because user \( i \) may be able to exploit channel \( j \)
if this channel is not available or not used by other users
\( i_1, i_2, \ldots, i_{MS} \). To estimate the increase of throughput, in
the remaining of this paper we are only interested in a
practical scenario where all \( p_{ij} \) are close to 1 (e.g., at least
0.8). This would be a reasonable assumption given several
recent measurements reveal that spectrum utilization of useful
frequency bands is very low (e.g., less than 15%). Under this
assumption, we will show that the increase-of-throughput for
user \( i \) can be estimated as

\[
\Delta T_{i}^{MS, ap}(j) = (1 - 1/MS)(1 - \delta)p_{ij}\left(\prod_{h \in S_i} \tau_{ih}\right)
\times \left(1 - \prod_{h \in S_{com}} \tau_{ih}\right) \sum_{k=1}^{MS} \left[\prod_{q=1, q \neq k}^{MS} p_{iqj}\right]
\times \prod_{q=1}^{MS} p_{iqj} \prod_{q=1}^{MS} \left(1 - \prod_{h \in S_{com}} \tau_{ih}\right)
\times (1 - 1/MS)(1 - \delta)p_{ij}\left(\prod_{h \in S_i} \tau_{ih}\right)
\times \prod_{q=1}^{MS} p_{iqj} \prod_{q=1}^{MS} \left(1 - \prod_{h \in S_{com}} \tau_{ih}\right)
\]  

This estimation is obtained by listing all possible scenar-
ios/events where user \( i \) can exploit channel \( j \) to increase its
throughput. Because the user throughput is bounded by 1, we
only count events that occur with non-negligible probabilities.
In particular, under the assumption that \( p_{ij} \) are high (or \( \tau_{ij} \)
are small) we only count events whose probabilities have at
most two such elements \( \tau_{ij} \) in the product. In addition, we can
determine the increase of throughput for user \( i \) by comparing
its achievable throughput before and after channel \( j \) is assigned
to it. It can be verified we have the following events for which
the average increases of throughput are significant:

- **Channel** \( j \) **is available** for all users \( i \) and \( q \), \( q = 1, 2, \ldots, MS \) except \( i_k \) where \( k = 1, 2, \ldots, MS \). In
  addition, all channels in \( S_i \) are not available and there
  is at least one channel in \( S_{com} \) available for user \( i \).

  User \( i \) can achieve a maximum average throughput of
  \( 1 - \delta \) by exploiting channel \( j \), while its minimum average
  throughput before being assigned channel \( i \) is at least
  \( (1 - \delta)/MS \) (when user \( i \) needs to share one available
  channel in \( S_{com} \) with MS other users). The increase of
  throughput for this case is \( (1 - 1/MS)(1 - \delta) \) and the
  upper-bound for the increase of throughput of user \( i \) is
  written in (5).

- **Channel** \( j \) **is available** for user \( i \) and all users \( i_q \),
  \( q = 1, 2, \ldots, MS \) but each user \( i_q \) uses other available
  channel in \( S_{iq} \) for his/her transmission. Moreover, there
  is no channel in \( S_{com} \) available. In this case, the increase
  of throughput for user \( i \) is \( 1 - \delta \) and the average increase
  of throughput of user \( i \) is written in (5).

- **Channel** \( j \) **is available** for user \( i \) and all users \( i_q \),
  \( q = 1, 2, \ldots, MS \) but each user \( i_q \) uses other available
  channel in \( S_{iq} \) for his/her transmission. Moreover, there
  is at least one channel in \( S_{com} \) available. In this case,
the increase of throughput for user \(i\) is upper-bounded by 
\((1 - 1/\mathcal{M}_S)(1 - \delta)\) and the average increase of throughput of user \(i\) is written in (7).

Detailed description of the algorithm is given in Algorithm 2. This algorithm has an outer and inter loops where the outer loop increases the parameter \(h\), which represents the maximum of users allowed to share any one particular channel (i.e., \(\mathcal{M}_S\) in the above estimation of the increase of throughput) and the inner loop performs channel allocation for one particular value of \(h = \mathcal{M}_S\). In each assignment iteration of the inner loop, we assign one “best” channel \(j\) to user \(i\) that achieves maximum \(\Delta T_h^{\text{up}}(j)\). This assignment continues until the maximum \(\Delta T_h^{\text{up}}(j)\) is less than a pre-determined number \(\epsilon > 0\).

### C. Calculation of Contention Window

We show how calculate contention window \(W\) so that collision probabilities among contending secondary users is sufficiently small. In fact, there is a trade-off between collision probabilities and the average overhead of the MAC protocol, which depends on \(W\). In particular, larger values of \(W\) reduce collision probabilities at the cost of higher protocol overhead and vice versa. Because there can be several collisions during the contention phase each of which occurs if two or more secondary users randomly choose the same value of backoff time. In addition, the probability of the first collision is largest because the number of contending users decreases for successive potential collisions.

Let \(\mathcal{P}_c\) be the probability of the first collision. In the following, we determine contention window \(W\) by imposing a constrain \(\mathcal{P}_c \leq \epsilon_P\) where \(\epsilon_P\) controls the collision probability and overhead tradeoff. Let us calculate \(\mathcal{P}_c\) as a function of \(W\) assuming that there are \(m\) secondary users in the contention phase. Without loss of generality, assume that the random backoff times of \(m\) secondary users are ordered as \(r_1 \leq r_2 \leq \ldots \leq r_m\). The conditional probability of the first collision if there are \(m\) secondary users in the contention stage can be written as

\[
\mathcal{P}_c^{(m)} = \sum_{j=2}^m \Pr\{j \text{ users collide}\} = \sum_{j=2}^m \sum_{i=0}^{W-2} C_m^j \left(\frac{1}{W}\right)^j \left(\frac{W - i - 1}{W}\right)^{m-j}. \tag{8}
\]

where each term in the double-sum represents the probability that \(j\) users collide when they choose the same backoff value equal to \(i\). Hence, the probability of the first collision can be calculated as

\[
\mathcal{P}_c = \sum_{m=2}^M \mathcal{P}_c^{(m)} \times \Pr\{m \text{ users contend}\}, \tag{9}
\]

where \(\mathcal{P}_c^{(m)}\) is given in (8) and \(\Pr\{m \text{ users contend}\}\) is the probability that \(m\) secondary users join the contention phase. To compute \(\mathcal{P}_c\), we now derive \(\Pr\{m \text{ users contend}\}\). It can be verified that secondary user \(i\) joins contention if all channels in \(\mathcal{S}_i\) are busy and there is at least one channel in \(\mathcal{S}_i^{\text{con}}\) available. The probability of this event can be written as

\[
\mathcal{P}_c^{(i)} = \Pr\{\text{all channels in } \mathcal{S}_i \text{ are busy, } \exists! \text{ some channels in } \mathcal{S}_i^{\text{con}} \text{ are available}\} = \prod_{j \in \mathcal{S}_i} \bar{p}_{ij} \left(1 - \prod_{j \in \mathcal{S}_i^{\text{con}}} \bar{p}_{ij}\right). \tag{10}
\]

The probability of the event that \(m\) secondary users join the contention phase is

\[
\Pr\{m \text{ users contend}\} = \sum_{n=1}^C \sum_{i \in \Lambda_n} \mathcal{P}_c^{(i)} \prod_{j \in \mathcal{S}_i^{\text{con}}} \mathcal{P}_c^{(j)} \tag{11}
\]

where \(\Lambda_n\) is one particular set of \(m\) users, \(\Lambda_M\) is the set of all \(M\) users \((\{1, 2, \ldots, M\})\). Substitute the result in (11) into (9), we can calculate \(\mathcal{P}_c\). Finally, we can determine \(W\) as

\[
W = \min\{W \text{ such that } \mathcal{P}_c(W) \leq \epsilon_P\} \tag{12}
\]

where for clarity we denote \(\mathcal{P}_c(W)\), which is given in (9) as a function of \(W\).

### D. Calculation of MAC Protocol Overhead

Let \(r\) be the average value of the backoff value chosen by any secondary user. Then, we have \(r = (W - 1)/2\) because the backoff counter value is uniformly chosen in the interval \([0, W - 1]\). As a result, average overhead can be calculated as follows:

\[
\delta(W) = [W - 1]/2 \times \theta + t_{\text{RTS}} + t_{\text{CTS}} + 3t_{\text{SIFS}}/T_{\text{cycle}}, \tag{13}
\]

where \(\theta\) is the time corresponding to one backoff unit; \(t_{\text{RTS}}, t_{\text{CTS}}, t_{\text{SIFS}}\) are the corresponding time of RTS, CTS and SIFS (i.e., short inter-frame space) messages; and \(T_{\text{cycle}}\) is the cycle time. Here, we have assumed that the sensing and synchronization internals in each cycle are very short, which are, therefore, ignored in the overhead calculation.

### E. Update \(\delta\) inside Algorithm 2

Because the overhead \(\delta\) depends on the channel assignment outcome, which is not known when we are running Algorithm 2. Therefore, in each allocation step we update \(\delta\) based on the current channel assignment outcome. Because \(\delta\) does not change much in two consecutive allocation decisions, Algorithm 2 runs smoothly in practice.

### V. Numerical Results

We present numerical results to illustrate the throughput performance of the proposed Algorithm 1 and 2. To test performance of both algorithms, the probabilities \(p_{i,j}\) are randomly realized in the interval \([0.7, 0.9]\). Other parameters are chosen as follows: cycle time \(T_{\text{cycle}} = 3\text{ms}\); \(\theta = 20 \mu s\), \(t_{\text{RTS}} = 48\mu s\), \(t_{\text{CTS}} = 40\mu s\), \(t_{\text{SIFS}} = 15\mu s\), and target collision probability \(\epsilon_P = 0.02\). In Fig. 2(a) we show total throughput \(T\) versus the number of channels \(N\) for \(M = 15\) obtained by both
Algs. 1 and 2 where each point is obtained by averaging the throughput over 30 different realizations of $p_{i,j}$. Throughput curves due to Algs. 1 and 2 are indicated as “P-ware” in the figures. In addition, for the comparison purposes, we also show throughput performance achieved by “P-blind” algorithms in Fig. 2(b) which simply allocate channels to users in a round-robin manner without considering particular values of $p_{i,j}$.

It can be seen that total throughput reaches the maximum value as the number of channels becomes sufficiently large, which confirms the result stated in Proposition 1. In addition, Alg. 2 achieves significantly larger throughput than Alg. 1 for lower values of $N$. This performance gain comes from the multiuser diversity gain, which arises due to the spatial dependence of white spaces.

As can be seen from Figs. 2(a) and 2(b) the proposed algorithms for both non-overlapped and overlapped cases outperform the round-robin channel assignment algorithms. For the non-overlapped case, Alg. 1 improves the total throughput significantly when comparing to the round-robin algorithm. For the overlapped case, we show throughput performance for the round-robin assignment algorithms when 2 and 5 users are allowed to share one channel (denoted as 2-user sharing and 5-user sharing in the figure). Although by allowing channel sharing among users, we can achieve larger throughput for the round-robin algorithm, they still perform worse compared to the proposed algorithms. We demonstrate the throughput gain due to Alg. 2 compared to Alg. 1 for different values of $N$ and $M$ in Fig. 3(a). This figure shows that performance gains up to 5% can be achieved by Alg. 2 compared to Alg. 1 when the number of channels is small or moderate. Moreover, we plot average probability of the first collision which is derived in Section IV.C versus contention window in Fig. 3(b). The outcomes of Alg. 2 make the collision probability first increases then decreases with $N$. In fact, as $N$ is relatively small or large compared to $M$, the number of users sharing same channels is small, which leads to small collision probability.

VI. CONCLUSION

We developed two channel assignment algorithms for throughput maximization in cognitive radio networks with hardware-constrained secondary users. The first algorithm performed non-overlapped channel assignment for secondary users, which was shown to achieve optimality if the number of channels is sufficiently large. In the secondary algorithm, we allowed overlapped channel assignments and designed a MAC protocol to resolve channel access contention when different users attempt to exploit the same available channel. We validated our results via numerical studies and demonstrated significant throughput gains of the overlapped channel assignment algorithm compared to the non-overlapped counterpart in different network settings.

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