Free Short-Period Internal Waves in the Arctic Seas of Russia

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Purpose. The aim of the work is to investigate vertical structure and phase characteristics of free short-period internal waves (IW), and to assess their dependence on density stratification in the Barents, Kara, Laptev and East Siberian seas.

Methods and Results. Solving the main boundary problem of the Sturm – Liouville theory resulted in calculating the amplitudes of velocity vertical component, own frequencies and periods of the first mode of internal waves. The density field was calculated using the reanalysis data (World Ocean Atlas 2018) on temperature and salinity for 1955–2017 with a resolution 0.25° × 0.25°. The relation between the internal waves’ vertical structure and dispersion features, and the density depth distribution was analyzed. It is shown that the averaged over the sea area depth of the maximum amplitude of the IW velocity vertical component in the Barents and Kara seas is ~ 90 m in the mid winter and ~ 75–80 m in summer, and in the Laptev and East Siberian seas – ~ 60 m throughout the entire year.

Conclusions. In the months when the density gradients are maximal, the internal waves of the highest frequency and the shortest period are observed. The maximum water stability in the Barents Sea takes place in July – August, in the Kara Sea – in July – September and November, in the Laptev Sea – in June, November, and in the East Siberian Sea – in July. Just in the same months, the maximum values of the averaged own frequencies, and the minimum values of the averaged own periods and amplitudes of the vertical component of the internal waves’ velocity are observed.

Keywords: Barents Sea, Kara Sea, Laptev Sea, East Siberian Sea, buoyancy frequency, internal waves, own frequency, own period, vertical component of velocity

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Introduction

One of the reasons for the appearance of internal waves (IW) in the ocean is the flow of tidal currents around bottom irregularities that result in periodic vertical displacements of isopycnic surfaces. In the ocean, these disturbances propagate in the form of free internal waves. However, when studying internal waves in the Arctic Basin, it the effect of critical latitude should be taken into account. A latitude close to 75° is critical for semidiurnal internal waves; to the north of this latitude, IW with a tidal frequency cannot exist in the form of free waves [1, 2]. Their generation mechanism at high latitudes is the same as at low and temperate ones, but at high latitudes the internal tidal wave is destroyed and generates packets of free short-period waves [3]. Several experimental observations of IW are described in the literature. They confirm the existence of internal short-period waves in the Arctic Basin: for example, in [4], IW were noted in the Barents Sea with periods of 15–60 min.
The present paper is aimed to study free short-period internal waves, the relationship between their vertical structure and phase characteristics with the Brunt – Väisälä frequency distribution over depth in the Barents, Kara, Laptev and East Siberian seas.

**Materials and Methods**

To calculate the monthly average values of density, the *World Ocean Atlas 2018* reanalysis data on temperature and salinity for the period 1955–2017 at 0.25°× 0.25° grids with a step of 5 m in depth to the 100 m horizon and with a step of 25 m – to 150 m horizon [5, 6] was used. Research area is 66–82°N, 16–180°E. The resulting density arrays were checked for inversions and, if necessary, corrected by inversion values’ replacement with values interpolated for adjacent horizons [7]. At each grid node, the buoyancy frequency profiles \( N(z) \) were calculated. The Brunt – Väisälä frequency maximum in depth \( (N_{\text{max}}(z)) \) and its depth \((HN_{\text{max}}(z))\) were determined.

The study of internal waves was carried out based on linear equations of motion of a continuously stratified fluid in the form of Fjeldstad [8], which have a solution in the form of a superposition of plane waves [9]. In particular, the vertical component of the velocity \( w(x, y, z, t) \) \((x, y \) are horizontal coordinates, \( t \) is time) is represented as follows

\[
    w(x, y, z, t) = \sum_{n=1}^{\infty} \int_{-\infty}^{\infty} W^{(n)}(k, z) \exp \left\{ i \left[ k_x x + k_y y - \omega^{(n)}(k) t \right] \right\} dk_x dk_y,
\]

where \( \omega^{(n)}(k) \) is the dispersion relation (own frequency) for mode with number \( n \) and wave number \( k = (k_x^2 + k_y^2)^{1/2} \); \( W^{(n)}(k, z) \) is this mode amplitude (eigenfunction). If the Boussinesq approximation is applied, to filter out surface waves and to neglect the Earth rotation, then \( W^{(n)}(k, z) \) will be a solution to a boundary value problem of the Sturm – Liouville type with zero boundary conditions at the bottom and free surface of the liquid:

\[
    \frac{d^2W^{(n)}}{dz^2} + \left( \lambda^{(n)} N^2 - k^2 \right) W^{(n)} = 0, \quad W^{(n)}(H) = W^{(n)}(0) = 0,
\]

where \( \lambda^{(n)} = (k/\omega^{(n)})^2 \), \( \omega^{(n)} \) is the own frequency; \( k \) is the wave number; \( H \) is the depth.

For the numerical implementation of the boundary value problem for a given profile \( N(z) \), its finite-difference approximation was constructed. The resulting system of linear algebraic equations was solved by a method based on solving the characteristic equation for its matrix [10].

It is known that the first mode makes the largest contribution to the energy spectrum of the wave packet; therefore, the amplitudes of the vertical velocity component \( W(z) \), own frequencies \( (\omega^{(1)}) \) and periods \( (T) \) of the first mode were considered [11]. To study the dispersion properties of IW, own frequencies were
calculated for wavelengths ($\lambda$) in the range of 250–1500 m with a step of 25 m. Presence of waves with lengths of $> 250$ m in the Arctic seas is confirmed by radar sensing from space [12]. The detail of IW manifestations in the radar images is limited by the pixel size of $75 \times 75$ m, and the minimum distinguishable wavelength is 250–300 m. Waves with shorter lengths in the images in the radar imaging modes indicated in [12] are difficult to determine.

**Analysis of the Results**

Despite the close geographical location of the Barents, Kara, Laptev and East Siberian seas, each of them has its own regional features, which are clearly illustrated in Fig. 1. For quantitative characterization and comparison of the intra-annual variability of water stratification, the average value of the Brunt – Väisälä frequency maximum ($N_{\text{max}}(z)_{\text{average}}$) in depth and the average depth of the maximum ($HN_{\text{max}}(z)_{\text{average}}$) for each sea were calculated.

It can be seen (Fig. 1, a) that the greatest density gradients in all the seas under consideration are observed in summer months, which is associated with ice melting and an increase in continental runoff. In the Barents Sea, the highest values of $N_{\text{max}}(z)_{\text{average}}$ are $\sim 12.4$ cycle/h, in the Kara and Laptev Sea – $\sim 35.8$ cycle/h and in the East Siberian Sea – $\sim 49.8$ cycle/h. The maximum water stability in the Barents Sea occurs in July – August, in the Kara Sea – in July – September and November, in the Laptev Sea – in June and November and in the East Siberian Sea – in July. The $N_{\text{max}}(z)_{\text{average}}$ values in the Barents Sea are several times lower than in other seas. The low water stability in the Barents Sea is explained by the North Cape Current influence. During its movement to the east, the Atlantic waters, having high salinity and temperature, cool and sink, which leads to a smoothing of the difference in density between the layers and to the stable equilibrium loss of the layers [13]. The river runoff into the Barents Sea is inconsiderable; however, almost half of the Kara and Laptev Sea area is located under the influence of continental waters. The decisive role in the formation of the hydrological conditions of these seas belongs to the processes occurring in the zones of mixing.
of surface Arctic waters with river waters. In areas of strong influence of river runoff, as a result of mixing of river and surface Arctic waters, water is formed with a relatively high temperature and low salinity. Large density gradients are created at their interface (horizon 5–10 m) [14]. The continental runoff into the East Siberian Sea does not affect its general hydrological regime significantly, but only determines some hydrological features of the coastal areas in summer. However, the East Siberian Sea is the most ice-covered of the Arctic seas, from October – November to June – July it is completely covered with ice. A significant increase in $N_{\text{max}(z)\text{average}}$ in July is apparently associated with increased ice melting in early summer [15].

Fig. 1, b shows the intra-annual variation of the own frequency of the IW first mode ($\omega_{\text{average}}^{(1)}$) averaged over the sea area. For a wavelength of 1000 m, the largest $\omega_{\text{average}}^{(1)}$ and the smallest own period of the first mode of the IW ($T_{\text{average}}$) averaged over the sea area in the Barents Sea are 1.41 cycle/h and 45 min; in the Kara Sea, 2.31 cycle/h and 30 min; in the Laptev Sea 2.32 cycles/h and 33 minutes and in the East Siberian Sea 2.19 cycles/h and 30 minutes. During the months of maximum density gradients, the highest frequency waves are observed. The correlation coefficient between the intra-annual cycles $N_{\text{max}(z)\text{average}}$ and $\omega_{\text{average}}^{(1)}$ exceeds 0.9 for all the seas.

The intra-annual variation of the first IW mode period averaged over the sea area is shown in Fig. 1, c. The values of the periods are presented for a wavelength of 1000 m, however, qualitatively, the $T_{\text{average}}$ graph will have the same form for other wavelengths from the range considered. The short-period waves are observed in the Kara and Laptev seas, for which $T_{\text{average}} (\lambda = 1000 \text{ m})$ averaged 12-month is 46 and 48 min, respectively, 87 min for the Barents Sea, 57 min for the East Siberian Sea. Fig. 1, 2 also show that IW with the shortest periods are observed in the months of the greatest density gradients. The correlation coefficient ($R$) between the intra-annual cycles $N_{\text{max}(z)\text{average}}$ and $T_{\text{average}}$ is approximately –0.95 for all the seas.

![Figure 2](image_url)
To analyze the vertical structure of the IW, the profiles of the amplitudes of the vertical components of the first IW mode velocity were calculated at each node of the grid. Also, the maximum amplitude of the vertical component of the velocity ($W_{\text{max}}(z)$) along the depth and the depth of its occurrence ($HW_{\text{max}}(z)$) were determined. Then, the $W_{\text{max}}(z)$ and $HW_{\text{max}}(z)$ values obtained for each month were averaged over the sea areas ($W_{\text{max}}(z)_{\text{average}}, HW_{\text{max}}(z)_{\text{average}}$) (Fig. 2). It was found that the highest values of $W_{\text{max}}(z)_{\text{average}}$ (more intense wave dynamics) are observed in the months of the lowest density gradients: in the Barents and Kara Seas – in March and in the Laptev and East Siberian seas – in April. The correlation coefficient between the intra-annual cycles $N_{\text{max}}(z)_{\text{average}}$ and $W_{\text{max}}(z)_{\text{average}}$ exceeds –0.9 for all the seas (Fig. 1, 2).

**Fig. 3.** Geographic distribution of maxima of the Väisälä – Brunt frequency and the amplitude of the vertical component of the IW first mode velocity (in conventional units) in August

Distribution of the Brunt – Väisälä frequency maxima and the amplitude of the vertical component of the first IW mode velocity in August is illustrated in Fig. 3, their depths are shown in Fig. 4. The waters with the greatest stability are located in coastal areas. The central and northern parts of the seas are occupied by waters with low values of the maximum buoyancy frequency. The most intense vertical wave motion of waters and the greatest depths of occurrence $N_{\text{max}}(z)$ and $W_{\text{max}}(z)$ are also observed there. The correlation coefficient between $N_{\text{max}}(z)$ and...
$W_{\text{max}}(z)$ is in the range $-0.47 \ldots -0.77$, between $H_{N_{\text{max}}}(z)$ and $H_{W_{\text{max}}}(z)$ – in the range $0.23–0.78$ (Fig. 5).

**Fig. 4.** Geographic distribution of depth of maxima of the Väisälä–Brunt frequency and the amplitude of the vertical component of the IW first mode velocity in August

**Fig. 5.** Correlation coefficients between $N_{\text{max}}$ and $W_{\text{max}}$ (solid line), and $HN_{\text{max}}$ and $HW_{\text{max}}$ (dashed line) for the Barents (turquoise curve), Kara (green curve), Laptev (blue curve) and East Siberian seas (red curve)
Fig. 6. Distribution over depth of the averaged over the sea area buoyancy frequency and amplitude of the velocity vertical component (in conventional units)
The Brunt – Väisälä frequency profiles and the amplitude of the vertical IW velocity component averaged over sea areas are shown in Fig. 6. It can be seen that the vertical density gradients in the Barents Sea are not large compared to other seas under consideration. Density jump layer is expressed from July to October, the depth of occurrence $N_{\text{max}}(z)_{\text{average}}$ is 20–30 m. Throughout the year, the vertical water dynamics is developed, which is the most pronounced in winter and spring. In the Kara Sea, density jump layer remains throughout the year. Due to the large volume of the Ob-Yenisei runoff, the values of the averaged Brunt – Väisälä frequency reach 31 cycles/h. In June, a seasonal pycnocline begins to form; from July to December, the density jump layer is pronounced. The depth of occurrence of the averaged $N_{\text{max}}(z)$ is 15–20 m. The Brunt – Väisälä frequency profile in September has a special form. At a depth of $\sim 15$ m, a sharp decrease in $N(z)_{\text{average}}$ is observed, and at 20–25 m horizon the buoyancy frequency reaches its maximum. Perhaps this is due to the onset of ice formation and convective mixing in the low salinity zone [16]. Vertical wave dynamics is less developed than in the Barents Sea. However, both in the Barents Sea and in the Kara Sea, the maximum $W(z)_{\text{average}}$ values are reached in winter and spring at 120–130 m horizons. In the Laptev and East Siberian seas, due to the runoff influence of the Khatanga, Lena, Kolyma, Indigirka rivers, as well as the freshened waters of the Siberian Coastal Current, the pycnocline can be traced throughout the year. In winter, spring and summer, the pycnocline layer reaches $\sim 100$ m, in autumn $\sim 70$ m. The highest value of $N(z)_{\text{average}}$ is determined in the East Siberian Sea in July and exceeds 45 cycle/h. The vertical wave motion of waters in the Laptev and East Siberian seas is less developed than in the Barents and Kara seas (Fig. 6).

To study the dependence of the vertical structure and phase characteristics of the IW on the wavelength, the averaged values of the amplitudes of the vertical component of the velocity for $\lambda > 250$ m were calculated (Fig. 7). The calculations were carried out for deep-water areas, where $H > 150$ m. It can be seen that with an increase in $\lambda$, the $W(z)_{\text{average}}$ values increase insignificantly, but the depth of occurrence of the maximum $W(z)_{\text{average}}$ remains unchanged. The largest $W(z)_{\text{average}}$ are observed in the Barents Sea. The depth of occurrence $W_{\text{max}}(z)_{\text{average}}$ is $\sim 90$ m in the Barents and Kara Seas in the middle of winter and 75–80 m in summer, in the Laptev and East Siberian Seas $\sim 60$ m throughout the year. The more intense vertical wave dynamics of the waters in the Barents Sea in comparison with other seas is due to the North Cape Current influence.

It can be seen (Figs. 7 and 8) that the averaged depths of occurrence $N_{\text{max}}(z)$ and $W_{\text{max}}(z)$ differ: for deep-water areas ($H > 150$ m) $H N_{\text{max}}(z)_{\text{average}}$ is in the layer of the seasonal pycnocline (15–40 m), $H W_{\text{max}}(z)_{\text{average}}$ – in the main pycnocline layer (60–90 m), i.e. $H N_{\text{max}}(z)_{\text{average}} < H W_{\text{max}}(z)_{\text{average}}$. 
Fig. 7. Intra-annual variability of the averaged over the sea area amplitude of vertical component of the IW first mode velocity (in conventional units) at $H > 150$ m and wavelengths 250, 500, 750, 1000 m (from left to right)
Fig. 8. Intra-annual variability of the averaged over the sea area buoyancy frequency in the Barents, Kara, Laptev and East Siberian seas (from left to right) at $H > 150$ m

Fig. 9 shows the intra-annual variability of the averaged dispersion dependences of the IW first mode in the Barents, Kara, Laptev and East Siberian seas (from left to right): $a$ – at $H > 150$ m; $b$ – for the entire water area

Fig. 9 shows the intra-annual variability of the averaged dispersion curves of the IW first mode in the 250–1500 m wavelength range, calculated for the deep-water region (Fig. 9, $a$) and the entire sea area (Fig. 9, $b$). The averaged dispersion dependences for the Barents Sea are practically the same, because the depths with $H < 150$ m are much smaller here than in the other three seas. For the Kara, Laptev and East Siberian seas, there are insignificant discrepancies in the short-wave area. The maximum averaged own frequencies of IWs in the Barents Sea are several times lower than in other seas.
Conclusion

Based on the World Ocean Atlas 2018 reanalysis data on temperature and salinity, an analysis of the vertical structure and dispersion properties of free internal waves was carried out and an assessment of the relationship between their characteristics and the Brunt–Väisälä frequency distribution over depth in the Barents, Kara, Laptev and East Siberian seas was fulfilled.

It is shown that the most intense dynamics of internal waves is observed in the Barents Sea. Due to the Atlantic Ocean influence, the vertical density gradients in the Barents Sea are small, and the amplitude of the vertical component of the wave velocity significantly exceeds $W(z)$ in other seas. The areas of the highest values of the amplitude of the vertical component of the velocity coincide with the areas of the lowest density gradients (central and northern areas of the seas). The correlation coefficient for sea areas between the maximum buoyancy frequency in depth and the maximum amplitude of the vertical velocity component is in the range of $-0.47 \ldots 0.77$, the correlation coefficient between the depths of their occurrence is in the range $0.23–0.78$.

The occurrence depth of the maximum amplitude of the vertical component of the IW velocity averaged over the Barents and Kara sea area is $\sim 90$ m in the middle of winter and $\sim 75–80$ m in summer; in the Laptev and East Siberian seas $\sim 60$ m throughout the year. The averaged depths of the Brunt–Väisälä frequency maximum are less than the averaged depths of the maximum amplitude of the vertical velocity component.

In the months of maximum density gradients, the highest frequency and short-period internal waves are observed. The maximum water stability in the Barents Sea is observed in July – August, in the Kara Sea – in July – September and November, in the Laptev Sea – in June and November and in the East Siberian Sea – in July. In the same months, the maximum values of the averaged own frequencies, the minimum values of the averaged own periods and amplitudes of the vertical component of the IW velocity are observed. The correlation coefficient modulus between the Brunt–Väisälä frequency maxima averaged over sea areas and the values of own frequencies, periods and amplitudes of vertical velocities exceeds 0.9.

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**Ekaterina A. Pavlenko** – analysis and validation of results, preparation of graphic materials, preparation of the paper text

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