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Dissociative electron attachment and vibrational excitation of CF$_3$Cl: Effect of two vibrational modes revisited

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We present a study of dissociative electron attachment and vibrational excitation processes in electron collisions with the CF$_3$Cl molecule. The calculations are based on the two-dimensional nuclear dynamics including the C-Cl symmetric stretch coordinate and the CF$_3$ symmetric deformation (umbrella) coordinate. The complex potential energy surfaces are calculated using the $ab$ initio $R$-matrix method. The results for dissociative attachment and vibrational excitation of the umbrella mode agree quite well with experiment while the cross section for excitation of the C-Cl symmetric stretch vibrations is about a factor of three low as compared to experimental data.

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I. INTRODUCTION

Dissociative electron attachment (DEA) to polyatomic molecules typically involves multidimensional nuclear dynamics. However, because of big computational work necessary to obtain multidimensional complex (i.e., including both real and imaginary parts) energy surfaces, most of theoretical DEA calculations were performed in one-dimensional approximation. In these calculations it is usually assumed that the DEA process involves one reaction (dissociating) coordinate, roughly corresponding to one of the normal modes of the target molecule. This approximation is sometimes too crude, and sometimes completely unjustified. Therefore, a lot of effort was devoted recently to calculations of multidimensional DEA dynamics [1–6]. These calculations address two important problems in the physics of DEA processes. First, we want to know which dissociation channels are the most important and what is the energy range where a particular bond breaking can occur. This information is especially important for chemical control. Second, we want to know the importance of different vibrational modes in a particular DEA process and the final-state vibrational energy distribution in the fragments.

The most common method for studies of dynamics on multidimensional surfaces is the wave-packet propagation technique [7]. Recently, this approach was used to calculate the DEA cross sections for several polyatomic molecules, e.g. for CO$_2$ [8] or H$_2$O [9], employing the multi-configuration time-dependent hartree (MCTDH) method [10, 11]. An alternative is to develop classical and semiclassical methods for treatment of nuclear dynamics. We recently reformulated [1] the quantum method for DEA in terms of the time-independent Schrödinger equation and connected this treatment with the classical approximation. The method was applied to the process

$$e + \text{CF}_3\text{Cl}(\nu_2, \nu_3) \rightarrow \text{CF}_3\text{Cl}^- \rightarrow \text{CF}_3(\nu'_3) + \text{Cl}^-.$$  \hspace{1cm} (1)

Here $\nu_2$ and $\nu_3$ stand for the symmetric deformation vibrations (so-called “umbrella” mode) and the symmetric stretch vibrations, $\nu'_3$ represents the umbrella mode of the free CF$_3$ radical. The two-mode approximation for this process can be justified by existing experimental data [12] on vibrational excitation (VE) of this molecule. The two-dimensional potential energy surface (PES) was calculated \textit{ab initio}. However, we used a model semiempirical width (the imaginary part of the complex PES). This led to some inconsistencies and instabilities in our calculations discussed below. In the present paper we employ the \textit{ab initio} molecular $R$-matrix method for calculation of the complex PES. This allows us to remove the deficiencies in our previous calculations and improve agreement with experimental data. We also calculate VE cross sections for the C–Cl symmetric stretch and the umbrella mode.

The rest of the paper is organized as follows. In Sec. II we discuss construction of the complex PES from the \textit{ab initio} calculations and the our theoretical approach to treatment of nuclear motion. In Sec. III we discuss details of our $R$-matrix scattering calculations in the fixed-nuclei approximation. In Sec. IV we present our results for DEA and VE.

II. THEORETICAL APPROACH

In our previous work [1] we constructed a two-dimensional local complex potential (LCP) model for DEA and resonant VE of CF$_3$Cl. The model takes into account the C–Cl stretching vibrational mode and umbrella vibrational mode of the CF$_3$ radical. The LCP model [1] was based on a complex PES constructed from the one-dimensional potential curves using an arbitrary extension in the coordinate corresponding to the umbrella vibrations of the CF$_3$ fragment. In addition, the real part of the complex potential curve for the temporal anionic complex was obtained using the \textit{ab initio} methods for bound-states calculations, while the imaginary part was obtained by fitting [13] the experimental results of Mann and Linder [12]. Cross sections of the DEA calculated using the two-dimensional model are factor of three higher than experimental values and one-dimensional non-local calculations [13]. This discrepancy was attributed to the inconsistencies between the real and imaginary part of the complex PES used in the model [1]. It is the aim of this work to construct a two-dimensional model of the nuclear dynamics along the same lines as in [1], however using a more consistent complex PES. We performed molecular \textit{ab initio} $R$-matrix scattering calculations in the fixed-nuclei approximation for a set of nuclear geometries including both degrees of freedom corresponding to the C–Cl distance $R$ and F–C–Cl angle $\vartheta$. We fitted the eigenphases obtained from these $R$-matrix calculations at energies close to the resonance position to the Breit-Wigner formula with an energy-dependent background [14] and using the resonance position and width we constructed the complex PES. This approach is free of any presumption on the dependence of the complex PES on the F–C–Cl angle and removes the need for any arbitrary extension in this coordinate used in [1]. In addition, the fixed-nuclei resonance width is calculated at the same level of the theory as the position.

The \textit{ab initio} molecular $R$-matrix method is well known and widely used for fixed-nuclei calculations of electron collisions with small and medium-sized molecules. We refer the reader to a recent review article by Tennyson [15] and to references therein for description of the method and its technical implementation.
The eigenphase sums calculated using the $R$-matrix method for a set of nuclear geometries were fitted using the Breit-Wigner formula taking into account the dominant dipole component of the potential in the outer region. The Breit-Wigner formula is equivalent to the one-pole approximation to the $R$-matrix [14]. This approximation is based on the assumption that at the energies close enough to the resonance position the $R$-matrix can be well approximated by the following expression:

$$R(E) = R_0 + \frac{\gamma_\lambda^2}{E - E_\lambda}, \quad (2)$$

where $R_0$ is the background $R$-matrix including all the terms due to remaining poles of the $R$-matrix, $E_\lambda$ is position of the pole closest to the resonance, $\gamma_\lambda$ is corresponding amplitude and $E$ is the scattering energy. To obtain the Breit-Wigner formula from Eq. (2), we assume that the term $R_0$ is a slowly varying function of energy as it is sum over all the other $R$-matrix poles. The eigenphase sum $\delta$ may then be expressed [14] as

$$\delta(E) = \tan^{-1}\left(\frac{1/3 \Gamma_\lambda}{E - E_\lambda + \Delta_\lambda}\right) - \phi(E), \quad (3)$$

where $\Gamma_\lambda$ is the resonance width and $\Delta_\lambda$ is the level shift (amount by which the resonance energy is shifted from the pole $E_\lambda$). The first term of Eq. (3) describes the resonance contribution and the second ($\phi(E)$) the potential scattering contribution. The relations between $\Gamma_\lambda$, $\Delta_\lambda$, $\phi$ and general solutions of the Schrödinger equation on the $R$-matrix boundary are given in Ref. [14]. In order to fit the width and the position of the resonance using this model we first solve the Schrödinger equation with the dipole potential in the outer region. The corresponding dipole moment for every nuclear geometry is obtained from the $ab$ initio calculation of target properties as a part of the fixed-nuclei scattering calculations. Having the solutions on the $R$-matrix boundary we can establish the relation between the background phase shift $\phi(E)$, width $\Gamma_\lambda$, level shift $\Delta_\lambda$ and quantities in Eq. (2). This allows us to fit the model $R$-matrix amplitude $\gamma_\lambda$, pole $E_\lambda$ and constant background $R$-matrix $R_0$ using the non-linear least-squares technique to the $ab$ initio eigenphase sum. These directly determine the width $\Gamma_\lambda$ and resonance energy $E_\lambda + \Delta_\lambda$. This fitting allows for a construction of the complex PES $U(R, r) - i\Gamma(R, r)/2$ in the region where the anionic state is metastable. In the region where the resonance turns into a bound state, the corresponding bound state energy was calculated as well as the potential energy curve $V(\infty, r)$ of the free CF$_3$ fragment. The complex PES was constructed using cubic splines in two dimensions. In order to study the final-state interaction on the anionic surface during the DEA process, it was necessary to have the bound anionic PES also for large C–Cl internuclear separations, where the $ab$ initio results are not available. It was constructed by the extrapolation of the $ab$ initio results as described in [1] to satisfy the condition $U(R \to \infty, r) \to V(\infty, r)$. The bound part of the anionic potential energy surface was extrapolated to match the CF$_3$ fragment potential curve asymptotically, as discussed in [1].

The LCP calculations of the DEA and VE presented here were performed in a similar way as described in Ref. [1]. The basic equation of the LCP theory reads

$$[T_\rho + T_r + U(\rho, r) - i\Gamma(\rho, r)/2 - E]\chi_E(\rho, r) = V_{\delta k}(\rho, r)\zeta_\nu(\rho, r), \quad (4)$$

where $\rho$ and $r$ are the reaction coordinates introduced to decouple the two-dimensional operator of the nuclear kinetic energy [1], $U(\rho, r) - i\Gamma(\rho, r)/2$ is the complex PES of the temporal anion, $V_{\delta k}(\rho, r) = \sqrt{\Gamma(\rho, r)/2\pi}$ is the amplitude for electron capture into the resonance state and $\zeta_\nu(\rho, r)$ is the vibrational wave function of the neutral molecule in the initial state. $T_\rho + T_r$ is the operator of nuclear kinetic energy corresponding to our two-dimensional model as discussed in [1]. In our previous work [1] the wave function $\chi_E(\rho, r)$ was expanded in the basis of vibrational states $\phi_\nu(r)$ of the CF$_3$ fragment in the harmonic approximation given by equation

$$[T_r + V^h(\infty, r) - \epsilon_\nu]\phi_\nu(r) = 0, \quad (5)$$

where $\epsilon_\nu$ are the corresponding eigenenergies $\epsilon_\nu = D_0 + \omega_3^f(\nu + 1/2)$, $\omega_3^f$ is the harmonic frequency of the CF$_3$ radical umbrella mode and $V^h(\infty, r)$ is the corresponding free CF$_3$ radical potential curve in the harmonic approximation with the minimum corresponding to the C–Cl bond dissociation energy. As it is explained in [1], projection of Eq. (4) on $\phi_\nu(r)$ then yields a set of coupled differential equations for channel wave functions of the variable $\rho$ with coupling potential $U_{\nu\nu'}(\rho)$ given by the equation

$$U_{\nu\nu'}(\rho) = \int \phi_\nu(r) \left[ U(\rho, r) - i\Gamma(\rho, r)/2 - V^h(\infty, r) \right] \phi_{\nu'}(r) dr. \quad (6)$$

One note should be made at this point regarding the asymptotic behavior of the coupling potential. The PES in [1] was extrapolated in such way that $U(R \to \infty, r) \to V(\infty, r)$. The extrapolation asymptotically matches the $ab$ initio
potential energy curve of the CF$_3$ fragment, not its harmonic approximation. As a consequence, $\lim_{\rho \to \infty} U_{\nu\nu'}(\rho) \neq 0$, as can be seen in Eq. (6). Since the coupling of different vibrational channels of the CF$_3$ radical doesn’t vanish for $\rho \to \infty$, population of different vibrational states of CF$_3$ produced by the DEA process does not converge well. This deficiency is corrected in the present work. The harmonic approximation for the potential energy curve $V^h(\infty, r)$ of the CF$_3$ radical is not used and the full $ab\ initio$ potential curve $V(\infty, r)$ is employed in both Eq. (5) and Eq. (6). Therefore, in our present calculations we expand the wave function $\chi_E(\rho, r)$ in the basis set of eigenfunctions $\varphi_\nu(r)$ given by the equation

$$[T_r + V(\infty, r) - \varepsilon_\nu] \varphi_\nu(r) = 0,$$

where $\varepsilon_\nu$ are the vibrational energies of the CF$_3$ fragment without the harmonic approximation. The corresponding coupling potential has the following form:

$$U_{\nu\nu'}(\rho) = \int \varphi_\nu(r) [U(\rho, r) - i\Pi(\rho, r)/2 - V(\infty, r)] \varphi_{\nu'}(r) dr.$$

Therefore, in the present work the extrapolated PES is consistent with the asymptotic treatment of the CF$_3$ fragment that allows for convergence of the population of vibrational states of CF$_3$ produced by the DEA process.

In the present work we also use a different method to solve the system of coupled radial equations. In Ref. [1] we used direct outward integration of the system of differential equations from the inner region and inward integration from the asymptotic region with subsequent matching of the solutions to satisfy the boundary conditions. The direct integration has a limitation in number of channels included in the calculation. With increasing number of closed channels, their exponentially increasing contribution starts to be more pronounced and the calculation becomes unstable.

Here we employ the multichannel version of the exterior complex scaling (ECS) method in the discrete variable representation (DVR) basis set [16], which is free of this problem. This method has previously been successfully used in the context of nonlocal resonance model for calculations of DEA and VE in case of diatomic molecules [17].

### III. SCATTERING CALCULATIONS IN THE FIXED-NUCLEI APPROXIMATION

In order to obtain the two-dimensional complex PES necessary to construct the LCP model, we performed the $R$-matrix scattering calculations in the fixed nuclei approximation for a set of nuclear geometries important for the DEA and VE. For every nuclear geometry we calculated the eigenphase sum in the energy interval around the fixed-nuclei resonance and fitted it to the Breit–Wigner formula with background as described above. The resonance position and width as a function of the nuclear coordinates represent the complex PES used in the local complex approximation. In the region where the CF$_3$Cl$^-$ anion is stable against autodetachment and the potential becomes real, the surface is represented by the bound-state energies calculated using the $R$-matrix approach.

As it was discussed previously [1], in our calculations the PES $V$ and $U$ for the neutral molecule and for the anion are represented using two coordinates: C-Cl internuclear separation $R$ and the distance between the C atom and the plane formed by the fluorine atoms $r = -R_{CF}\cos\vartheta$, where $\vartheta$ is the F-C-Cl angle and $R_{CF}$ is the F-C bond length. Since we do not include the C-F stretching mode into our considerations, $R_{CF}$ is fixed and set to the value 1.342 Å corresponding to the equilibrium geometry of the neutral CF$_3$Cl. The fixed-nuclei $R$-matrix calculations were performed for a two-dimensional region of nuclear coordinates with $R$ from 3 $a_0$ to 12 $a_0$ and with $\vartheta$ from 55° to 90°. In the present work we consider excitation of the low vibrational states of the CF$_3$ fragment only, therefore we don’t take into account any effects caused by the flipping of the radical ($\vartheta > 90^\circ$).

Calculations were performed using Gaussian type orbitals (GTOs) and the UK polyatomic $R$-matrix code [15]. The highest symmetry available in the polyatomic code is $C_s$, which is an abelian subgroup of the true $C_{3v}$ symmetry of CF$_3$Cl.

#### A. Target representation

The CF$_3$Cl was represented using Hartree–Fock (HF) molecular orbitals (MOs). In order to construct a target model sufficient for the purpose of the dynamical calculations, we performed several tests with different target models to select the best compromise between the quality of the target representation and the computational tractability of the $(N + 1)$-particle problem.

The CF$_3$Cl target states were represented using a complete active space (CAS) configuration interaction (CI) wave function. The CF$_3$Cl molecule contains 50 electrons. Only 18 of them belong to the inner shells, 32 remaining electrons
form the valence shells and in principle can contribute to the chemical bonds. This complicates the construction of the target CI model in several aspects. Enough valence electrons should be included in the CI active space to treat the electron correlation properly. In addition, it is necessary to treat the target symmetrically and to ensure that all elements of the degenerated pairs of MOs are included in the CAS. On the other hand, inclusion of each orbital occupied in the HF ground state leads to a rapid increase in dimension of the target and anionic CI Hamiltonians. In addition, it is the aim of our fixed-nuclei calculations to study the dependence of the resonance on the nuclear geometry. This raises further the limitations on the $N+1$-particle CI calculation as we need to repeat it many times.

The first CAS CI target model considered in our calculations includes eight active electrons which occupy four orbitals in the HF ground state determinant with the highest orbital energies. We allow these electrons to occupy five lowest virtual orbitals (VOs). Using the notation of the $C_s$ point group, this CAS model can be expressed as follows:

$$ (1a' \ldots 15a')^{30}(1a'' \ldots 6a'')^{12}(16a' \ldots 21a', 7a'' \ldots 9a'')^8 $$

or

$$ (1a' \ldots 15a')^{30}(1a'' \ldots 6a'')^{12}(16a' \ldots 20a', 7a'' \ldots 10a'')^8, $$

as the ordering of VOs changes with nuclear geometry. Using the notation of the $C_{3v}$ point group, the active electrons are taken from the following set of HF orbitals: $(1a_2, 10a_1, 7e)$. The degenerated $e$-orbitals in this set are well localized on the chlorine atom, the $10a_1$-orbital is spread along the C–Cl bond and the $1a_2$ orbital contributes to the C–F bonds. The calculations were performed using the 6-311G* GTO basis set [18, 19].

Representation of the target in the subsequent scattering calculation can be qualified by comparison of several properties calculated using our model with the previously published results. To check our target representation, we calculated the vertical excitation energy (as the excited target states are used in the scattering calculations), dipole moment of the target ground state (as it represents the major contribution to the interaction with the projectile in the outer region) and static dipole polarizability which allows us to estimate the representation of the polarization effects in the scattering calculation. Comparison of values calculated using our models (at equilibrium nuclear geometry) with the previously published data is shown in Table I. As it can be seen there, this target model (denoted as Model

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|}
\hline
 & Model 1 & Model 2 & Bibliographical data \\
\hline
GTO basis & 6-311G* & cc-pVDZ & \\
\# of active electrons / # of VOs & 8/5 & 4/11 & \\
\hline
Ground state energy (a.u.) & $-795.787343$ & $-795.627044$ & \\
Vertical excitation energy $^1E$ (eV) & 9.545 & 9.057 & $7.7 \pm 0.1$ [20, 21] \\
Vertical excitation energy $^3E$ (eV) & 8.476 & 7.897 & \\
Dipole moment (a.u.) & 0.378 & 0.410 & 0.197 [22] \\
Static dipole polarizability (a.u.) & 1.32 & 0.158 & 38.6 [22] \\
\hline
\end{tabular}
\caption{Target properties calculated using different CAS CI models at equilibrium nuclear geometry and their comparison with the previously published results.}
\end{table}

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|}
\hline
 & Model 1 & Model 2 & Bibliographical data \\
\hline
$\omega_2$ (cm$^{-1}$) & 854.42 & 956.48 & 775.12 [23] \\
$\omega_3$ (cm$^{-1}$) & 433.08 & 534.13 & 463.33 [23] \\
CF$_3$ fragment ($\omega_2$) (cm$^{-1}$) & 755.53 & 745 & 701 [24] \\
\hline
\end{tabular}
\caption{Vibrational frequencies calculated using different CAS CI models and their comparison with the previously published results.}
\end{table}

1 there and elsewhere in the text) gives a reasonably good representation of the ground state dipole moment, as it is relatively small, although our calculation gives us a larger value than found in the experiment. The vertical excitation energy calculated here is almost 2 eV higher than the experimental value [21]. It suggests that the representation of the target excited states is limited. According to our knowledge, there is no experimental or advanced theoretical calculation of the lowest excited state $^3E$ available. Our target model gives its energy 8.453 eV above the ground
state. In our scattering calculations, we are interested in scattering energies below 4 eV, where all the electronically excited channels are closed. We expect (and our test calculations described below suggest it) that inclusion of the lowest excited target states in the close-coupling (CC) expansion leads to a small correction of the resonance position and width only.

In order to estimate how well are the polarization effects represented in our scattering calculations, we evaluated the static dipole polarizability of the target ground state. We used the sum-over-states formula with the set of target states included in the scattering calculation. We found that the lowest six target states represent a considerable contribution. Adding more target states did not increase the value. As can be seen in Table I, our calculated value is considerably smaller than the experimental results. Since the higher excited states do not have significant contribution to the polarizability, this discrepancy can be possibly attributed to low number of active electrons and orbitals used in our target model. Good representation of the polarizability would require presence of more diffuse MOs which are too high in energy to be included in the present target calculations. However, the previously published one-dimensional calculations of the nuclear dynamics for CF$_3$Cl [13] show that the polarization effects have a minor effect on the results of the LCP calculations.

Target properties discussed above are all calculated at the equilibrium nuclear geometry. However, for our calculations of the nuclear dynamics it is important to know how well can our target model reproduce the harmonic vibrational frequencies of the neutral molecule. Comparison of our calculated values with the previously published result is showed in Table II. Our target model 1 gives the values with 10% accuracy when compared with the experimental results. This small difference can be possibly attributed to the neglect of other vibrational degrees of freedom in our model.

We can conclude that our CAS CI model 1 represents the neutral target sufficiently enough to be used in our ab initio R-matrix calculation. R-matrix calculations performed at the equilibrium nuclear geometry can be used to obtain the vertical attachment energy. Correct value of this quantity is essential for our calculations of the resonant nuclear dynamics. However, the CAS CI model 1 of the target leads to the value which is 1.3 eV above the experimental value determined by Aflatooni and Burrow [25]. Additional testing calculations show that it is due to insufficient treatment of the electron correlation in the CC expansion of the $N+1$-electron wave function. Since further increase of the number of active electrons or VOs included in the target model leads to intractable diagonalization of the $N+1$-electron Hamiltonian, we decided to model the electron correlation by modification of the primary GTO basis set, where we modified the gaussian exponent corresponding to the p-orbital of the chlorine atom in order to get the energy of the lowest unoccupied molecular orbital (LUMO) closer to the experimental value of the vertical attachment energy. We expect that this modified LUMO helps to represent the discrete component of the resonant wave function of the temporal anionic complex better than the linear combination of VOs obtained in model 1. This idea is similar to the method developed in Ref. [26] used to calculate the position and width of the resonance. The modified HF orbitals were calculated using the cc-pVDZ GTO basis set [27]. To approach the correct value of vertical attachment energy we changed the exponent of the uncontracted p-orbital of chlorine from 0.162 to 0.094. In addition to this modification of the exponent, we also restricted the CAS CI model to four active electrons from the highest occupied molecular orbital (HOMO) and HOMO-1 and allowed their excitations into 11 lowest VOs. Using the notation of the $C_s$ point group, this CAS model can be expressed as follows:

$$(1a' \ldots 16a')^{32}(1a'' \ldots 7a'')^{14}(17a' \ldots 25a', 8a'' \ldots 11a'')^4$$  \hspace{1cm} (11)$$

or

$$(1a' \ldots 16a')^{32}(1a'' \ldots 7a'')^{14}(17a' \ldots 24a', 8a'' \ldots 12a'')^4,$$  \hspace{1cm} (12)$$
as the ordering of VOs changes with nuclear geometry. Therefore, in this model we extend the space of VOs and reduce the number of active electrons as compared with model 1. Properties of the target calculated at the equilibrium nuclear geometry are summarized in Table I (we refer to this model as to Model 2 in the table and elsewhere in the text below). It shows that although the ground state energy is higher than the value calculated using model 1, the vertical excitation energy into the $^1E$ state is lower and closer to the published reference value. This CAS model of the target also gives lower vertical excitation energy to the $^3E$ state than model 1. Table I also shows that this modified model gives larger value of the vertical attachment energy than model 1, however its value is still low enough to not to introduce a significant error in the position and width of the resonance. We also calculated the static dipole polarizability at equilibrium nuclear geometry using this model and found that its value is significantly smaller than that given by experiment. This can be due to the limited representation of the polarization effects by the primary GTO basis set. Although both our CAS models of the target have their limitations, model 2 using the modified primary GTO basis represents correctly the vertical attachment energy, the quantity which is essential for the DEA calculations.

In addition to the CAS model of the target we need a representation of the CF$_3$ fragment in our LCP calculations in order to extrapolate the potential energy surfaces properly. In order to keep the model of the fragment consistent
with the target model 2, we treated the CF$_3$ radical at the SCF level as all the excitations of the active electrons in model 2 of the CF$_3$CI target describe the C–Cl chemical bond. Therefore, any CI excitation model of the fragment would introduce a correlation which is not explicitly included in the target model. In order to check the quality of this representation we calculated the harmonic frequency of the umbrella mode. Its comparison with previously published value is given in Table II. It shows that our calculated harmonic frequency is slightly higher than the experimental value, but they are in a good agreement to confirm that our model is a suitable choice for representation of the CF$_3$ radical.

B. Scattering model

The $R$-matrix calculations were performed using a sphere with radius $r_0=15\,\text{a.u.}$. Corresponding continuum basis set was represented by single-center uncontracted GTOs with exponents optimized by the program GTOBAS [28]. Partial waves up to $l = 3$ (9s, 7p, 7d, 7f) were used. The deletion threshold in the orthogonalization procedure for the continuum orbitals [15] was set to $\delta_{thr} = 9 \times 10^{-6}$. This value was found by performing calculations in the static exchange approximation. It gives a stable representation of the scattering continuum and does not show any problems related to linear dependence of the continuum orbitals.

In order to obtain the position and width of the fixed-nuclei resonance as a function of the nuclear geometry we performed a scattering calculation of the eigenphases and fitted them using the Breit-Wigner formula with the energy dependent background [14] as discussed above. We tested both CAS CI models of the neutral target discussed above. First, the lowest 16 CI target states calculated using Model 1 were used in the CC expansion and the $R$-matrix calculation at equilibrium nuclear geometry. This calculation gives converged results with respect to the number of target states included.

The corresponding cross section for elastic $^2A_1$ scattering is presented in Fig. 1 where we also compare it with calculations of Beyer et al. [29]. This curve (designated as Target model 1) shows the peak at energy around 3.3 eV that is significantly above the experimental value due to experimental work by Underwood-Lemons et al. [30] and the theoretical calculation of Beyer et al. [29]. Since a further increase of the number of target states included in the CC expansion did not lead to any considerable shift of the peak towards lower energies, it suggests that this artificially high position of the resonance is not due to incorrect representation of the polarization effects [31], but rather due to an incompleteness of the target model. Therefore, we performed another set of scattering calculations using target CI model 2 described above. Since this model was constructed to reproduce the correct vertical attachment energy, it also gives the correct position of the resonance peak in the $R$-matrix calculation carried at the equilibrium nuclear geometry (as plotted in Fig. 1). The rapid increase of the cross section at lower energies is due to the long-range dipole potential included in the outer region. For a molecule with a nonzero permanent dipole moment and fixed orientation the elastic cross section diverges at zero energy [32, 33], the feature which is observed in our cross section, but not in the calculation of Beyer et al. [29], apparently because the dipole effects were not included completely there. On the other hand, since our dipole moment at the equilibrium internuclear separation is too big (see Table I), it is evident that our elastic cross sections are strongly overestimated at low energies.

There were 12 target states included in our CC expansion (three lowest in singlet and triplet state of $A'$ and $A''$ symmetries). The $R$-matrix was propagated in the dipole potential given by the target CAS CI model (as discussed above) and in the potential given by the dipole and quadrupole coupling of different scattering channels [15]. On the other hand, the $R$-matrix calculation of Beyer et al. [29] was performed at the level of static exchange with polarization which treats the electron correlation in a different way than our CAS CI model. This can be a partial reason of the quantitative difference between the two calculations at higher energies.

Fig. 1 also presents the experimental measurements of the total elastic cross sections by Underwood-Lemons et al. [30]. However, the problem with this and two other [12, 34] measurements for CF$_3$Cl is that it is not quite clear what is measured there. The total elastic cross section for a polar symmetric top is divergent even if rotations are included [35]. Only the inversion splitting, which is extremely small for CF$_3$Cl, makes the elastic cross section finite [36]. This means that the scattering amplitude at small scattering angle $\theta$ behaves like $1/\theta$, and only at an extremely small angle $\theta_{inv}$ it becomes finite. In the experiment of Underwood-Lemons et al. [30] the elastic cross section is determined from the transmitted current under the assumption that transmitted electrons are not scattered, therefore what is measured in fact is the cross section integrated from a small angle $\theta_{min}$ to $180^\circ$, where $\theta_{min}$ is determined by the geometry of the experimental apparatus, and $\theta_{min}$ is, most likely, significantly greater than $\theta_{inv}$. In the experiment of Mann and Linder [12] the total cross section is obtained by extrapolating the measured differential cross section to $\theta = 0$. This procedure also gives an underestimated total cross section since the actual differential cross section behaves as $1/\theta^2$ at small angles, if $\theta > \theta_{inv}$. We think, therefore that comparison between the theory and the experiment for the total (integrated) cross section is meaningless unless the angle $\theta_{min}$ can be found from the experimental geometry. The purpose of plotting the experimental cross section in Fig. 1 is to demonstrate that our calculated resonance
FIG. 1. (Color online) Cross section for the elastic electron scattering off CF$_3$Cl ($^2A_1$ symmetry) calculated in the fixed-nuclei approximation at equilibrium nuclear geometry. Calculations employing target model 1 is compared with results calculated using model 2, with experimental results [30] and with other $R$-matrix calculation [29].

contribution is consistent with experimental results.

At larger C–Cl separations, where the resonance turns into a bound state, the corresponding anionic bound state energies were calculated by diagonalizing the $N + 1$ electron Hamiltonian constructed using the same target and scattering CAS CI model as was used for calculation of the resonance, just the integrals involving continuum GTOs were not restricted to the inner region of the sphere [15]. This allows a good representation of the diffuse character of the anionic bound state with energy close to the autodetachment limit.

The position and width of the fixed-nuclei resonance as a function of the nuclear geometry were obtained by fitting the eigenphases at energies close to the resonance to the Breit-Wigner formula with energy-dependent background performed at each nuclear geometry of our interest. The energy dependence of the background is predominately determined by the dipole moment of the neutral target. The corresponding value was obtained from the calculation of the target properties for every nuclear geometry and used as a parameter in the fitting procedure for this geometry. Fitting of the eigenphases calculated at equilibrium geometry using target model 2 gives a resonance position 1.954 eV, which is in a good correspondence with experimental value 1.83 eV due to Aflatooni and Burrow [25].

IV. CALCULATIONS OF THE NUCLEAR DYNAMICS

A. Dissociative electron attachment

The total DEA cross section calculated using our two-dimensional LCP approach is plotted in Fig. 2. This graph shows its comparison with previously published one-dimensional non-local calculations [13]. Our previously published
Two-dimensional LCP calculations [1] give significantly larger magnitude of the total DEA cross section than experimental works [25, 37] and one-dimensional non-local semiempirical calculation [13]. This problem was attributed to incorrect dependence of the width function (which was arbitrarily extended to two dimensions) on the coordinate $r$. As can be seen in Fig. 2, results of our present two-dimensional LCP calculations using the complex PES constructed from the $R$-matrix results are in very good agreement with the non-local calculations as well as with experimental results due to Aflatooni and Burrow [25]. Although our total cross section is smaller than the experimental results of Underwood-Lemons et al. [37], it is closer to the measurements of Aflatooni and Burrow [25], and the position of the peak is in very good correspondence with this experimental work. All this suggests that the two-dimensional PES constructed from the results of the $R$-matrix calculations has more correct dependence on both reaction coordinates than the previously published model [1]. It results in a correct shift of the peak in the total DEA cross section with respect to the VAE as well as in the correct magnitude of the cross section. One additional note regarding the complex PES should be made here. The DEA cross section is related to the position of the crossing seam between the neutral and anionic PES. Its shape and position with respect to the minimum of the neutral PES determine where the anionic system becomes stable. Subsequently, it has an influence on the survival probability. The crossing seams obtained from the present $R$-matrix calculations and from the model potential [1] are compared in Fig. 3. The relative position of the crossing seam is similar in both models. This supports our argument that the difference in magnitude of the DEA cross section between our present model and the results published in [1] is mainly due to the different width function $\Gamma(\rho, r)$, rather than due to the substantial difference in the crossing seam between these two models. The oscillatory structure in the crossing seam obtained from the present $R$-matrix calculations is mainly an artifact of too low density of the grid of nuclear geometries used to calculate the PES. In addition, the fact that the complex energies in the region, where the anion is metastable are obtained in different way than the energies of the bound anion, also raises the numerical issues with exact determination of the crossing seam and partially also contributes to
FIG. 3. (Color online) The crossing seam between the neutral and anionic two-dimensional PES obtained from the present R-matrix calculations and its comparison with model potential used in [1]. The cross (circle) denotes the equilibrium geometry of the neutral PES obtained in the present work (used in [1]).

Comparisons of local two-dimensional and one-dimensional results with nonlocal one-dimensional results are given in Refs. [1, 38]. The agreement between the local and non-local results is very good because the resonance occurs at a relatively large energy, and the long-range interaction plays a minor role.

Fig. 4 shows the distribution of different final vibrational states of the CF$_3$ fragment calculated using the complex PES constructed from the R-matrix results. In Fig. 5 we show the distribution calculated using the PES obtained in Ref. [1] but corrected in such a way that PES in the intermediate region smoothly turns into the PES in the asymptotic region avoiding the mismatch discussed in Sec. II. Both graphs show that the low vibrationally excited states of the CF$_3$ fragment will be more populated than the ground state and in both figures the positions of the peaks rise with increasing quantum number $\nu$. However, each calculation predicts highest population for a different excited state. While our complex PES constructed from the R-matrix results gives the highest peak for $\nu = 1$, the PES described in [1] leads to the highest peak for vibrational state $\nu = 3$, as can be seen in Fig. 5. Total DEA cross section is mainly determined by the complex PES in the region where the anionic system is not bound and does not strongly depend on the behavior of the PES in the region where the negative ion is stable. On the other hand, the distribution of vibrational states of the fragment is strongly influenced by the final-state interaction in the region where the anion is stable. In both calculations shown in Fig. 4 and Fig. 5, this region of the PES was partially modeled (as discussed above and in [1]) to achieve correct asymptotic behavior of the potential. Although our PES constructed from the R-matrix results is free of several limitations of the surface described in [1], the extrapolation of the bound-state anionic surface in both cases makes it difficult to decide, how quantitatively reliable this distribution is in both calculations.
B. Vibrational excitation

Results of the resonant VE calculations using the PES based on the R-matrix results are plotted in Fig. 6. This figure shows the cross section for VE of the target from the ground state to the lowest excited state of the C–Cl stretching mode (denoted as (0, 1) in the figure) and the lowest excited state of the C–F deformation mode (denoted as (1, 0) in the figure). These graphs show a very good agreement with our previous calculations [1] for both vibrational modes. However, our calculations agree with experimental results by Mann and Linder [12] for the umbrella mode, while both our models lead to approximately three times smaller magnitude of the cross section for the C–Cl stretching mode excitation than that measured by Mann and Linder [12].

The previously published one-dimensional non-local calculation of VE [13] takes into account the C-Cl stretching vibrational mode only and the width function $\Gamma(R)$ was adjusted to give cross sections corresponding to experimental results for this stretching vibrational modes excitation due to Mann and Linder [12]. The low values of the present cross sections can be partially explained by introduction of additional channels of vibrational excitation in our two-dimensional calculations and lower flux towards the channel (0, 1).

Although Fig. 6 shows that the model constructed using the R-matrix results leads to VE cross sections very similar to those calculated in Ref. [1], Fig. 7 shows that these two models predict different results for higher final vibrational states. To our best knowledge, there are no experimental data for VE to these states to compare with our cross sections. The fact that the differences between our two models become more significant with increasing final vibrational state is understandable, since the target vibrational eigenfunctions become spatially more extended with increasing vibrational state ($\nu_2, \nu_3$). This means that the different behavior of corresponding complex PES farther from equilibrium will have larger influence on results, as can be seen in Eq. (4).
FIG. 5. (Color online) DEA cross sections for different final vibrational states of the fragment CF$_3$ calculated using the model complex PES published previously [1] after the correction of the asymptotic behavior of channel potentials.

V. CONCLUSION

The \textit{ab initio} \textit{R}-matrix method allowed us to calculate the complex two-dimensional PES for CF$_3$Cl collisions. We used then DVR method to obtain the solution of coupled stationary equations (4), and DEA and VE cross sections for the e–CF$_3$Cl collision process. Our results for the total DEA cross section and the cross section for VE of the umbrella mode agree quite well with experiments. In addition we obtained the final-state vibrational distribution in the CF$_3$ fragment free of instabilities found in our previous calculations. However our cross sections for VE of the C-Cl stretching mode are significantly lower than the experimental results of Mann and Linder [12] and the results of previous semiempirical one-dimensional calculations [13]. This is something one might expect because of the extra inelastic channels of excitation of umbrella mode that leads to a redistribution of the flux. However, disagreement of the present 2-dimensional results with the experiment is puzzling and requires a further investigation.

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FIG. 6. (Color online) VE cross sections from the ground vibrational state to the lowest excited state of the C-Cl stretching mode (a) and the lowest excited state of the umbrella mode (b). Results calculated using the $R$-matrix complex PES are compared with cross sections obtained from the previously published model [1] and experimental results due to Mann and Linder [12].
FIG. 7. (Color online) VE cross sections for excitation from the target vibrational ground state to higher excited states. Results obtained from the complex PES constructed from the $R$-matrix results (solid line) are compared with cross sections calculated using the PES described in [1] (dashed line).
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