Heat-Capacity Measurements of Energy-Gap Nodes of the Heavy-Fermion Superconductor CeIrIn$_5$ Deep inside the Pressure-Dependent Dome Structure of its Superconducting Phase Diagram

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We use heat capacity measurements as a function of field rotation to identify the nodal gap structure of CeIrIn$_5$ at pressures to 2.05 GPa, deep inside its superconducting dome. A four-fold oscillation in the heat capacity at 0.3 K is observed for all pressures but with its sign reversed between 1.50 and 0.90 GPa. On the basis of recent theoretical models for the field-angle dependent specific heat, all data, including the sign reversal, imply a $d_{x^2-y^2}$ order parameter with nodes along $[110]$, which constrains theoretical models of the pairing mechanism in CeIrIn$_5$.

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The Ce-based heavy-fermion family CeMIn$_5$ (M=Rh, Co, Ir) has attracted attention due to their exotic properties and interesting interplay between magnetism and superconductivity$^1$. CeRhIn$_5$ is antiferromagnetic (AFM) at ambient pressure but becomes superconducting as pressure suppresses the AFM order and tunes CeRhIn$_5$ to a quantum-critical point (QCP)$^2$, indicating an intimate relationship between AFM fluctuations and unconventional superconductivity. CeCoIn$_5$, with the highest superconducting $T_c$=2.3 K among Ce-based heavy-fermion materials$^3$, is a nodal superconductor with a $d_{x^2-y^2}$ order parameter (OP) that is revealed consistently in a variety of experimental measurements$^4$. Cd or Hg doping, acting as an effective negative pressure, tunes the ground state of CeCoIn$_5$ from superconducting to AFM$^4$$^5$. The resulting temperature-doping phase diagram is very similar to the temperature-pressure diagram of CeRhIn$_5$, revealing a common response of these materials to the interplay between magnetism and superconductivity. CeIrIn$_5$ is also superconducting at ambient pressure with bulk $T_c$~0.4 K but resistive $T_c$~1.2 K$^6$$^7$. This difference in $T_c$ is found as well when magnetic order coexists with superconductivity in CeRhIn$_5$ and doped CeCoIn$_5$$^8$, but there is no low-range AFM in CeIrIn$_5$. Further, the response of CeIrIn$_5$ to effective pressure is different, as shown in the inset of Fig.1(a). Rh-doping in CeRh$_2$Ir$_{1-x}$In$_5$ acts as an effective negative pressure and induces a dome of superconductivity in proximity to AFM at $x$$\geq$0.5. $T_c$ goes to zero or approximately zero at $x$~0.1 before it rises again with applied pressure to form a second dome$^9$$^{10}$$^{11}$. This diagram is very similar to that of CeCu$_2$(Si$_{1-x}$Ge$_x$)$_2$ as a function of pressure$^{11}$ and has led to the suggestion that the second superconducting dome (SCII), so distant from AFM order and thus less associated with AFM fluctuations$^{11}$, may be due to another pairing mechanism, such as Cevale fluctuations$^{12}$, and possibly supports a different OP symmetry.

Identifying the nodal gap structure and pairing symmetry in CeIrIn$_5$ is an important step toward resolving the pairing mechanism. Power laws in heat capacity, thermal conductivity$^1$ and penetration depth$^2$ are consistent with line nodes in the gap, but these do not probe the node positions, which is needed to determine the allowed OP symmetry. A large anisotropy between in-plane and out-of-plane thermal conductivity measurements on CeIrIn$_5$ has led to a proposed hybrid gap, $k_z(k_x+ik_y)$$^{21}$$^{22}$. In contrast, thermal conductivity studies in a magnetic field that is rotated within the basal plane imply a $d_{x^2-y^2}$ gap with line nodes along the $[110]$ direction$^{22}$, similar to CeCoIn$_5$$^9$ and CeRhIn$_5$ under pressure$^{24}$. This discrepancy may be due in part to both measurements being made at ambient pressure where the superconductivity of CeIrIn$_5$ sits right at the margin of the two superconducting domes and may be influenced by the competition between residual AFM fluctuations and other pairing interactions, if any. Probing the gap structure in the superconducting state deep inside SCII avoids these complications.

In this Letter, we report heat capacity measurements of CeIrIn$_5$ under pressures up to 2.05 GPa as a magnetic field is rotated around and through its tetragonal c-axis. A four-fold oscillation of the in-plane heat capacity indicates a gap of $d_{x^2-y^2}$ symmetry with nodes along $[110]$, even deep inside SCII. This OP symmetry should be captured in mechanistic models of superconductivity of CeIrIn$_5$ in SCII.

CeIrIn$_5$ single crystals were grown out of In-rich flux and screened by magnetic susceptibility to ensure the absence of free In. The sample was mounted in a Be-Cu/NiCrAl hybrid clamp-type pressure cell with silicone fluid as the pressure-transmitting medium, which provides a very nearly hydrostatic environment to 25 kbar. The resistive superconducting transition temperature of Sn was measured to determine the pressure at low temperatures. The heat capacity of CeIrIn$_5$ $C_{ac}$ under pressure was measured by an ac calorimetric method wherein heating from an ac current generates an oscillation in the
sample temperature $\Delta T_{ac}$ that is measured by a field-calibrated Cr/AuFe (0.07%) thermocouple through its ac response; the heat capacity is inversely proportional to $\Delta T_{ac}$, i.e., $C_{ac} \propto 1/\Delta T_{ac}$. Magnetic field rotation was provided by a triple-axis vector magnet that accommodates a $^3$He cryostat with the pressure cell inside.

FIG. 1: (color online). (a) Temperature-dependent heat capacity of CeIrIn$_5$ at pressures $P=2.05$ GPa (circles), 1.50 GPa (diamonds) and 0.90 GPa (stars) normalized to the values at $T=1.8$ K. The inset is the phase diagram of Ce(Ir,Rh)In$_5$ as a function of Rh doping and pressure, taken from Ref. 25. (b) Heat capacity of CeIrIn$_5$ at $T=0.3$ K and $P=2.05$ GPa as a function of magnetic field applied along [001] (squares), [100] (diamonds) and [110] (circles) direction, respectively.

Figure 1(a) shows the temperature dependence of the heat capacity $C_{ac}$ under pressures $P=0.9$, 1.5 and 2.05 GPa going deeper into SCII with increased bulk $T_c=0.50$, 0.75 and 0.85 K, respectively. The magnetic field-dependent heat capacity $C_{ac}$ is shown in Fig. 1(b) for CeIrIn$_5$ at $0.3$ K and 2.05 GPa with the field applied along three major crystallographic orientations: [001], [100] and [110]. The upper critical field along the c-axis $H_{c2}^{[c]}$ is smaller than that within the ab plane by a factor of 2, similar to the case of CeCoIn$_5$ 26 and CeRhIn$_5$ 24.

Within the ab plane, $H_{c2}^{[ab]}$ along [100] is reproducibly a little larger than $H_{c2}^{[110]}$ in the [110] direction, probably reflecting the $d$-wave superconducting OP symmetry as discussed later.

Figure 2 shows the field-angle heat capacity of CeIrIn$_5$ at 2.05 GPa deep inside SCII with magnetic field rotated in the ab (ac) plane. For the field rotated within the ab plane, $C_{ac}/T$ is featureless in the normal state at 1.8 K even with magnetic field up to 8.0 kG. An apparent four-fold oscillation is present in $C_{ac}^{(\phi)}$ when cooling down to 0.3 K in the superconducting state and applying field at 2.0 kG. A polar sweep at 0.3 K with $H=2.0$ kG is shown in Fig. 2(b) and a two-fold modulation is observed, which can be fitted to the function $C_{ac}(\theta) = C_0 + C_2|\cos \theta|$, most likely caused by the $H_{c2}$ anisotropy between c-axis and ab plane.

Theoretical and experimental progress has established field-angle dependent heat capacity (and thermal conductivity) as a powerful probe of nodal locations in the superconducting gap structure $\delta E \sim p_F \cdot v_s$, where $p_F$ is the Fermi momentum of QPs and $v_s$ is the supercurrent velocity. In nodal superconductors at low temperatures, the Doppler energy shift plays an important role in the QP excitations. Near the nodes, the local superconducting gap is sufficiently small that the Doppler shift breaks Cooper pairs, $\Delta(p_F) < |p_F \cdot v_s|$, and, consequently, the QP density of states (DOS) depends on the field orientation relative to the position of gap nodes. In a classical picture, the QP DOS and thus heat capacity is a minimum for the field along nodal directions and a maximum along antinodal directions. In the case of a $d$-wave superconductor, a four-fold oscillation emerges in the superconducting state when the field is rotated in the basal plane and the local heat capacity minimum reflects a nodal position on the Fermi surface 29. The four-fold oscillation observed in an azimuthal field sweep for CeIrIn$_5$ at 2.05 GPa implies the presence of vertical line nodes perpendicular to the
ab-plane as expected for a gap with d-wave symmetry. A hybrid gap with horizontal line nodes in the equator is inconsistent with the four-fold oscillation observed here.

The angular location of maxima and minima in $C_{ac}(\phi)$ allows a distinction in the OP symmetry between $d_{xy}$ and $d_{x^2-y^2}$. Figs. 3 (a)-(d) show the heat capacity $C_{ac}$ of CeIrIn$_5$ at 2.05 GPa and 0.3 K as a function of field angle $\phi$ against the [100] direction in the ab plane at different fields up to 9.5 kG. Data at 9.5 kG (Fig. 3 (d)) are qualitatively different from those at lower fields (Figs. 3 (a)-(c)): at 9.5 kG local minima are shifted by 45 degrees and the oscillation amplitude is one order of magnitude larger relative to those in (a)-(c). We note that this magnetic field is very close to $H_{c2}$ for [100] and [110] directions. The in-plane $H_{c2}$ anisotropy will contribute four-fold oscillation in $C_{ac}(\phi)$ with local minima in [110] directions, providing an indirect way to check the crystalline orientation. The offset of $C_{ac}$ between [110] and [110] in Fig. 3 (d) indicates a small sample misalignment between the crystal ab-plane and the field xy-plane, which introduces a two-fold oscillation in the field rotation heat capacity. The total heat capacity in magnetic field can thus be written as $C_{ac}(\phi)=C_0+C_2\cos(2(\phi-\phi_0))+C_4\cos(4\phi)$, where $C_0$ is the zero-field heat capacity coming from thermally excited QPs and phonons, the two-fold term is due to the sample misalignment, and the four-fold oscillation $C_4\cos(4\phi)$ arises from nodal structure of the superconducting OP.

Though the local minima of $C_{ac}(\phi)$ are all in the [100] direction and maxima are along [110] for different magnetic fields as shown in Fig. 3 (a)-(c), the naive classical picture would imply a $d_{xy}$ OP symmetry with line nodes along [100] directions for CeIrIn$_5$ at 2.05 GPa. However, Vorontsov and Vekhter have argued that the classical picture holds only when $T/T_c \ll 1$ and $H/H_{c2} \ll 1$, and, consequently, the angular dependence of four-fold oscillations shows a complex evolution across the whole H-T phase diagram. In general, anisotropic scattering of QPs due to vortices produced by the magnetic field plays an important role in the DOS variation and thus the heat capacity as a function of the field orientation, which is missed in the classical picture. At an intermediate temperature or moderately high field, angular anisotropy in the heat capacity changes sign and the four-fold oscillation is inverted, showing maxima rather than minima when the field is along the nodal direction. According to their calculation of the field-angle dependent heat capacity of CeCoIn$_5$, where a corrugated cylindrical FS is assumed, our field rotation heat capacity measurements at 0.3 K, with $T/T_c \sim 0.35$, are in the intermediate region of the H-T phase diagram and a four-fold component with maxima in the nodal directions is expected. Our observation of oscillation maxima in [110] directions for CeIrIn$_5$ at 2.05 GPa indicates that the line nodes are along diagonals of the crystal lattice and favors $d_{x^2-y^2}$ symmetry over $d_{xy}$ for CeIrIn$_5$ at 2.05 GPa deep inside SCII. Similar behaviors observed for CeIrIn$_5$ at 1.50 GPa with $T/T_c \sim 0.40$ (not shown here) also are consistent with a $d_{x^2-y^2}$ OP symmetry.

This interpretation is supported by results plotted in Figs. 3 (e)-(g) that show the field-rotation heat capacity $C_{ac}$ of CeIrIn$_5$ at 0.90 GPa and 0.3 K as a function of field angle $\phi$ for $H=2.0$, 3.5 and 5.0 kG, respectively. In contrast to the data at 2.05 GPa, four-fold oscillations at 2.0 and 3.5 kG are inverted and show minima along [110]. Figure 3 (h) is a plot of the normalized four-fold oscillation amplitude $C_4/\Delta C(H)$ as a function of normalized field $H/H_c$ at 0.3 K for CeIrIn$_5$ at 2.05, 1.50 and 0.90 GPa, where $\Delta C(H)=C(H)-C(0)$ is the change of heat capacity in magnetic field. With similar amplitudes (3 - 6%), the four-fold oscillations have the same sign at 2.05 and 1.50 GPa but a different sign at 0.90 GPa. We summarize all of our results at different pressures and magnetic fields and compare them to the theoretical expectations in Fig. 4. This comparison assumes the similarity between CeCoIn$_5$ and CeIrIn$_5$ mentioned.
above. While the measurements at 2.05 and 1.50 GPa are located in the intermediate region, the points at 0.90 GPa and T/T_c ∼ 0.6 are near the boundary of the low H/H_c2, high T/T_c shaded region where the four-fold oscillation switches its sign again from that expected in the intermediate region and exhibit minima for field in the nodal directions. We note that the detailed division of different regions depends on the exact shape of the Fermi surface, and the general trend of sign change from intermediate to high temperature ranges should survive \cite{31}. Consequently, oscillation minima along [110] for CeIrIn_5 at 0.90 GPa also are consistent with d_{x^2-y^2} OP symmetry.

An interesting point is that we observe an in-plane upper critical field anisotropy, with H_c2 in the [110] direction always smaller than along [100] for all pressures. On the basis of model calculations in Ref. \cite{31}, this upper critical field anisotropy between nodal and antinodal direction appears naturally as a result of the d-wave gap symmetry with H_{node} < H_{antinode}. We also stress that the in-plane H_{c2} anisotropy cannot be the origin of the observed four-fold heat capacity oscillation because the oscillation change its sign between 2.05 and 0.90 GPa but the in-plane H_{c2} anisotropy remains the same. We thus conclude that the line nodes are in [110] directions and the gap symmetry of CeIrIn_5 stays d_{x^2-y^2} across SCII.

Because of proximity to AFM order, it is natural to consider that the OP symmetry in SCI is d_{x^2-y^2} as it is in CeCoIn_5 or CeRhIn_5 under pressure, which also are near AFM order. On the other hand, our field-rotation heat capacity results also favor d_{x^2-y^2} gap symmetry deep inside SCII, up to 2.05 GPa. In this regard, recent transport measurements observe non-Fermi liquid behaviors and claim that AFM fluctuations survive deep inside SCI \cite{27}. It is then an interesting question why the superconducting phase apparently is divided into two regions but with the same gap symmetry. One possible scenario is that there is some hidden competing order that destroys bulk superconductivity in CeIrIn_5 near ambient pressure and produces a minimum in the bulk superconducting transition temperature. More studies are required to clarify the origin of two superconducting domes in the CeIrIn_5 system.

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