Temporally Correlated Task Scheduling for Sequence Learning

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Abstract

Sequence learning has attracted much research attention from the machine learning community in recent years. In many applications, a sequence learning task is usually associated with multiple temporally correlated auxiliary tasks, which are different in terms of how much input information to use or which future step to predict. For example, (i) in simultaneous machine translation, one can conduct translation under different latency (i.e., how many input words to read/wait before translation); (ii) in stock trend forecasting, one can predict the price of a stock in different future days (e.g., tomorrow, the day after tomorrow). While it is clear that those temporally correlated tasks can help each other, there is a very limited exploration on how to better leverage multiple auxiliary tasks to boost the performance of the main task. In this work, we introduce a learnable scheduler to sequence learning, which can adaptively select auxiliary tasks for training depending on the model status and the current training data. The scheduler and the model for the main task are jointly trained through bi-level optimization. Experiments show that our method significantly improves the performance of simultaneous machine translation and stock trend forecasting.

1. Introduction

Sequence learning (Sutskever et al., 2014; Bahdanau et al., 2014) is an important problem in deep learning, which covers many applications including machine translation (Wu et al., 2016; Vaswani et al., 2017), time series prediction (Qin et al., 2017a; Zhang et al., 2017a), weather forecasting (Shi et al., 2015; Kim et al., 2017), etc. In real-world applications, a sequence learning task is often associated with multiple temporally correlated tasks: (1) In simultaneous machine translation, we need to begin translation before reading the complete source sequence. In this application, the generation of output sentence is $k$ word behind the source input, which is called wait-$k$ strategy/task (Ma et al., 2019). Wait-$k$ tasks with different $k$ values are temporally correlated. (2) Stock forecasting aims to predict the trend of stocks at some future day (Dai & Zhang, 2013). Tasks of predicting stock prices at different future days constitute a set of temporally correlated tasks. Different from general multi-task learning, the input and output data of these temporally correlated tasks are highly overlapped, and only differ in how much future input to use when processing the current input (e.g., how many future source words to read to translate the current word in simultaneous translation) or which future data to predict (e.g., the price movement of which future day to predict in stock trend forecasting).

Clearly, a given sequence learning task (denoted as the main or target task) can be boosted by its temporally correlated tasks. Taking English-to-Vietnamese simultaneous translation as an example, assume the main task is wait-3, and the temporally correlated tasks are wait-1, 2, 3, ···, 13. By training a model on all those correlated tasks and evaluating the model on wait-3, we observe that the BLEU score is improved from 27.17 to 28.54. (BLEU (Papineni et al., 2002) is a widely used accuracy metric in machine translation, the larger the better.) A similar phenomenon is observed in stock price forecasting. Improvements across various applications motivate us to explore how to leverage those temporally correlated tasks more effectively to improve performance on the main task.

Given that there are usually multiple temporally correlated tasks, the key challenge lies in which tasks to use and when to use them in the training process. In this work, we introduce a learnable task scheduler for sequence learning, which adaptively selects temporally correlated tasks during the training process. The scheduler accesses the model status and the current training data (e.g., in current minibatch), and selects the best auxiliary task to help the training of the main task. The scheduler and the model for the main task are jointly trained through bi-level optimization: the scheduler is trained to maximize the validation performance of the model, and the model is trained to minimize the training loss guided by the scheduler. Experimental results on simultaneous machine translation and stock trend forecasting show
that such a task scheduler brings significant improvements.

Our main contributions are three-fold:

(1) To the best of our knowledge, we are the first to formulate and study the problem of leveraging temporally correlated tasks for sequence learning.

(2) We propose a new learning algorithm with a scheduler to adaptively select the temporally correlated tasks to boost the main task. The scheduler and the model of the main task are jointly trained without additional supervision signals.

(3) We empirically verify the effectiveness of our method. Experiments on four simultaneous translation tasks show that our method improves wait-k baseline by 1 to 3 BLEU scores. Experiments on a stock price forecasting dataset show that our method can improve the baselines in terms of Spearman’s rank correlation coefficient and prediction loss.

Our code for simultaneous translation task is at https://github.com/shirley-wu/simul-mt_temporally-correlated-task-scheduling, and the code for stock price forecasting is at https://github.com/microsoft/qlib/tree/main/examples/benchmarks/TCTS.

# 2. Problem Setup and Our Algorithm

In this section, we first set up the problem of temporally correlated task scheduling for sequence learning, and then present our algorithm. Finally, we discuss the connection between our method and existing methods, and also provide an intuition why our method works.

## 2.1. Problem Setup

Let $X$ and $Y$ denote the input space and output space, and let $\mathcal{T} = \{T_1, \cdots, T_{|\mathcal{T}|}\}$ denote a set of temporally correlated tasks. Depending on applications, those tasks can be temporally correlated in different ways. We categorize them into two main classes and formalize them as follows.

(1) **Sequence processing with latency constraints**: Tasks in this category aim to process each token in an input sequence, one by one sequentially, under certain latency constraints. Representative examples include simultaneous translation (Ma et al., 2019), which targets at translating each source word without waiting for the end of the input sentence, and streaming speech recognition (He et al., 2019), which requires recognizing each word said by a speaker in real-time, etc.

Let $x$ denote an input sequence and $x_t$ denotes its $t$-th token. We focus on the setting where each token in $x$ will be sequentially processed. Each task $T \in \mathcal{T}$ is associated with a non-negative integer $\delta_T$, indicating that when processing the token $x_t$, how many additional tokens can be used. Note that in conventional sequence learning where the complete source sequence is available, $\delta_T = \infty$. In the extreme case where no latency is allowed, $\delta_T = 0$. Let $f_T$ denote the model for task $T$, which generates the output sequentially. $\hat{y}$ denotes the output sequence of $f_T$ based on $x$, and is initialized as an empty list. After processing $x_t$, conditioned on $x_{\leq t+\delta_T}$, $x\in \{x_1, x_2, \cdots, x_{t+\delta_T}\}$, based on the processed representations of $x_t$, $x_{\leq t+\delta_T}$, and the already generated $\hat{y}$, $f_T$ needs to make a decision $\hat{y} = f_T(x, x_{\leq t+\delta_T}, \hat{y})$. The decision could be to generate a single token, multiple tokens, or no token. After that, we append $\hat{y}$ to the end of $\hat{y}$. We repeat the above steps to process all tokens in $x$.

(2) **Predicting the future**: Tasks in this category aim to predict some future values for a given time series. Representative examples include stock trend forecasting (Dai & Zhang, 2013), where we want to predict the price trend of an individual stock on some future days (e.g., tomorrow, the day after tomorrow, etc.) based on its historical prices, and weather forecasting (Shi et al., 2015; Kim et al., 2017), where we want to predict the weather of a city on a future day based on its historical weather.

Let $x$ denote the input time series, and $y = (y_1, y_2, \cdots)$ denote the output sequence, where $y_t$ is the value of the $t$-th future day/step. For a task $T \in \mathcal{T}$, the goal is to predict the value of the $\sigma_T$-th future day, i.e., $\tilde{y}_{\sigma_T}$, where $\sigma_T$ is a positive integer and varies across different tasks $T$.

Each task has a different loss function $\ell(x,y,T)$, which is used to measure the distance between the predicted $\hat{y}$ and the groundtruth $y$ (in the first class of tasks) or $\tilde{y}_{\sigma_T}$ and $y_{\sigma_T}$ (in the second class of tasks). Any task in $\mathcal{T}$ can be the main task, and the others are regarded as auxiliary tasks. In this work, our goal is to better leverage those auxiliary tasks to help the main task.

## 2.2. Our Algorithm

As aforementioned, our basic idea is to introduce a task scheduler, which adaptively selects an auxiliary training task to improve the performance of the main task. A basic assumption of our algorithm is that the models for all tasks in $\mathcal{T}$ can share parameters (except for a few individual parts like task embeddings), which is easy to satisfy in machine translation, stock trend forecasting, etc. Let $f(x; \theta)$ denote the model with parameter $\theta$. Let $\phi(x, y, \theta; \omega)$ denote the task scheduler parameterized by $\omega$, which outputs an auxiliary task in $\mathcal{T}$ conditioned on an input-output pair $(x, y)$ and the model $f(\cdots; \theta)$ of the main task. More specifically, we extract a low-dimensional feature $I_{x,y,\theta}$ to describe $(x, y, \theta)$ and use it as the actual input of the scheduler network $\phi$. For ease of reference, we will alternatively use $\phi(x, y, \theta; \omega)$ and $\phi(I_{x,y,\theta}; \omega)$. $\phi$ can be different functions depending on applications, which will be discussed in Section 3 and 4.
Figure 1: The optimization workflow of one episode. The solid lines and dashed lines represent the workflow of inner-optimization (w.r.t. \( \theta \)) and outer-optimization (w.r.t. \( \omega \)) respectively. At step \( s \), with training data \((x_s, y_s)\), the scheduler \( \varphi(x_s, y_s, \cdot) \) chooses a suitable task \( T_s \) (green solid lines) to update the model \( f(x_s, \cdot; \theta) \) (blue solid lines). After \( S \) steps, we evaluate the model \( f \) on the validation set \( D_v \) and update the scheduler \( \varphi \) (green dashed lines).

Now we have two sets of parameters to learn from the data: \( \omega \) in the scheduler \( \varphi \) and \( \theta \) in the model \( f \). Let \( D_t \) and \( D_o \) denote the training and validation sets respectively. We formulate the training of \( f \) and \( \varphi \) as a bi-level optimization (Sinha et al., 2017), which is

\[
\max_{\omega} M(D_v; \theta(\omega)) \quad \text{s.t.,} \quad \theta(\omega) = \arg\min_{\theta} \frac{1}{|D_t|} \sum_{(x,y) \sim D_t} E_{T \sim \varphi(x,y,\cdot;\omega)} \ell(x,y,T;\theta).
\]

In the above formulation, \( M(D_v; \theta(\omega)) \) denotes the validation performance of the main task, and \( \ell \) is the loss function of data \((x,y)\) on task \( T \). Intuitively, we expect that the scheduler can select a good auxiliary task for each input-output pair, so that eventually the validation performance of the model on the main task can be maximized.

Following the common practice (Liu et al., 2019; Fan et al., 2018), we optimize Eqn.(1) in an alternative way: We first fix \( \omega \) and optimize \( \theta \), and then fix \( \theta \) and optimize \( \omega \) using the REINFORCE algorithm (Sutton & Barto, 2018). We repeat the process until convergence, as shown in Algorithm 1. The training process consists of \( E \) episodes (i.e., the outer loop), and each episode consists of \( S \) update iterations (i.e., the inner loop). The inner loop (from step 4 to step 9) aims to optimize \( \theta \), where we can update the parameter with any gradient-based optimizer like momentum SGD, Adam (Kingma & Ba, 2015), etc. The outer loop (from step 2 to step 11) aims to optimize \( \omega \). \( \varphi(x,y,\cdot;\omega) \) can be regarded as a policy network, where the state is the feature \( I_{x,y,\cdot} \), the action is the choice of task \( T \in T \), and the reward is the validation performance \( R_v \) (step 10). At the end of each episode, we update \( \omega \) using REINFORCE algorithm (step 11). The workflow of one episode is shown in Figure 1.

### 2.3. Discussion

Our problem is related to several other learning settings.

1. In multi-task learning (Zhang & Yang, 2017) (briefly, MTL), multiple tasks are jointly trained and mutually boosted. In MTL, each task is treated equally, while in our setting, we focus on the main task.

2. Transfer learning (Pan et al., 2010) also leverages auxiliary tasks to boost a main task. Curriculum transfer learning (briefly, CL) (Shao et al., 2018; Dong et al., 2017) is one kind of transfer learning which schedules auxiliary tasks according to certain rules, e.g., from easy to difficult. Our problem can also be regarded as a special kind of transfer learning, where the auxiliary tasks are temporally correlated with the main task. Our learning process is dynamically controlled by a scheduler rather than some pre-defined rules.

3. Our method is also related to Different Data Selection (DDS) (Wang et al., 2020). Both our work and DDS train a meta controller to improve the learning process on a given task via reinforcement learning. The main difference is that DDS aims to better select training data from a dataset, while our work aims to better utilize temporally correlated data.
tasks (and their corresponding data). Given a main task, our method constructs and schedules a series of temporal correlated tasks, while DDS works on the given task only.

Intuitively, training with temporally correlated auxiliary tasks helps the main task for two reasons: (1) The temporally correlated tasks either share the same output with overlapped inputs or the same input. Thus, joint training of them enables shared representation learning, just like general multi-task training (MTL), and consequently improves the main task; (2) The $x/y$ pairs from correlated tasks can be viewed as noised augmentation of the training data for the main task, which helps the main task.

3. Application to Simultaneous Translation

3.1. Task Description

Simultaneous neural machine translation (briefly, NMT) has attracted much attention recently. In contrast to standard NMT, where the NMT system can access the full input sentence, simultaneous NMT requires the model to conduct translation before reading the full input sentence. In this task, $X$ and $Y$ are collections of sentences in the source language and the target language. Wait-$k$ (Ma et al., 2019) is a simple yet effective method in simultaneous NMT, where the translation is $k$ words behind the source input. Formally, given a data pair $(x, y) \in X \times Y$ where the $t$-th token of $x/y$ is $x_t/y_t$, when we read a prefix $(x_1, x_2, \cdots, x_k)$ (briefly denoted as $x_{\leq k}$), we need to output the first target token $y_1$: when reading $x_{k+1}$, we should output $y_2$, etc. In comparison, for standard NMT, one can start translation after reading all tokens in $x$. A larger $k$ makes the task easier and leads to better translation quality, but at the cost of a larger waiting time.

Under our framework, simultaneous translation belongs to the first class of tasks in Section 2.1. Let $T_m$ denote wait-$m$ task, and $\delta_{T_m}$ for task $T_m$ is $m-1$. Assuming wait-$k$ is the main task $T_{main}$, then the temporally correlated tasks $\mathcal{T}$ are wait-$m$ with different $m$ values, i.e. $\mathcal{T} = \{T_1, T_2, \cdots, T_M\}$. In this work, we set $M = 13$. If the scheduler $\varphi$ assigns a task $T_m$ (i.e., wait-$m$) to a data pair $(x, y)$, the loss function on this task is:

$$
\ell(x, y; T_m, \theta) = \sum_{t=1}^{\left|y\right|} \log P(y_t | y_{\leq t-1}, x_{\leq t+m-1}; \theta).
$$

3.2. Background

Previous work on simultaneous NMT can be categorized by whether using a fixed decoding strategy or an adaptive one. Fixed strategies use pre-defined rules to determine when to read or to write a new token (Dalvi et al., 2018; Ma et al., 2019). Wait-$k$ is a representative method (Ma et al., 2019), which achieves good results in terms of translation quality and controllable latency, and has been used in speech-related simultaneous NMT (Zhang et al., 2019; Ren et al., 2020).

For adaptive strategies, Cho & Esipova (2016) proposed wait-if-worse (WIW) and wait-if-diff (WID) methods which generate a new target word if its probability does not decrease (for WIW) or if the generated word is unchanged (for WID) after reading a new source token. Grissom II et al. (2014) and Gu et al. (2017) used reinforcement learning to train the read/write controller, while Zheng et al. (2019a) trained the controller in a supervised way. Alinejad et al. (2018) added a “predict” operator to the controller so that it can anticipate future source inputs. Zheng et al. (2019b) introduced a “delay” token into the target vocabulary indicating that the model should read a new word. Monotonic infinite lookback attention (MILk) used a hard attention model to determine when to read new tokens, and a soft attention model to perform translation (Arivazhagan et al., 2019). Ma et al. (2020) introduced multi-head attention to MILk and proposed monotonic multihead attention (MMA) with two variants: MMA-IL (Infinite Lookback) with higher translation quality and greater computational overhead, and MMA-H(ard) with higher computational efficiency. Besides, Zheng et al. (2020a) extended wait-$k$ to an adaptive strategy by training multiple wait-$m$ models with different $m$’s and adaptively selecting a decoding strategy during inference. Zheng et al. (2020b) explored a new setting, where at each timestep, the translation model over-generates the target words and corrects them in a timely fashion.

3.3. Settings

Datasets: For IWSLT’14 En→De, following (Edunov et al., 2018), we split 7$k$ sentences from the training corpus for validation, and the test set is the concatenation of tst2010, tst2011, tst2012, dev2010 and dev2012. For IWSLT’15 En→Vi, following (Ma et al., 2020), we use tst2012 as the validation set and tst2013 as the test set. For IWSLT’17 En→Zh, we concatenate tst2013, tst2014 and tst2015 as the validation set and use tst2017 as the test set. For WMT’15 En→De, following (Ma et al., 2019; Arivazhagan et al., 2019), we use news2013 as the validation set and use news2015 as the test set. More details about datasets can be found in Appendix C.1.

Models: Following Ma et al. (2019), the translation model $f$ is based on Transformer (Vaswani et al., 2017). However, different from Ma et al. (2019), we conduct incremental encoding, so that when encoding each source token, the model can only attend to its previous tokens. The computation complexity for encoding is $O(L_x^3)$ compared to $O(L_x^2)$ in Ma et al. (2019), where $L_x$ is the length of the source sentence $x$. We find that our model is more efficient than Ma et al. (2019) with little accuracy drop. Detailed formulation and empirical comparison are in Appendix B.
For IWSLT En→Zh and En→Vi, we use the transformer small model, where the embedding dimension, feed-forward layer dimension, number of layers are 512, 1024 and 6 respectively. For WMT’15 En→De, we use the same architecture but change the embedding dimension into 256. For WMT’15 En→De, we use the transformer big setting, where the above three numbers are 1024, 4096 and 6 respectively. The scheduler \( \varphi \) for each task is a multilayer perceptron (MLP) with one hidden layer and the \( \text{tanh} \) activation function. The size of the hidden layer is 256.

**Input features of \( \varphi \):** The input of \( \varphi \) is a 7-dimension vector with the following features: (1) the ratios between the lengths of the source/target sentences to the average source/target sentence lengths in all training data (2 dimensions), i.e., \( L_x/\sum_{x' \in X} L_{x'}/|X| \) and \( L_y/\sum_{y' \in Y} L_{y'}/|Y| \); (2) the training loss over data \((x, y)\) evaluated on the main task \( \text{wait-} k \); (3) the average of historical training losses; (4) the validation loss of the previous epoch; (5) the average of historical validation loss; (6) the ratio of current training step to the total training iteration. The ablation study of feature selection is in Appendix E.1.

**Choice of \( \mathcal{M} \):** The validation performance \( \mathcal{M} \) is the negative validation loss with \( \text{wait-} k \) strategy. To stabilize training, the reward for the \( e \)-th episode (step 10 of Algorithm 1) is \( R_e - R_{e-1} \), where \( R_{e-1} \) is the validation performance \( \mathcal{M} \) of the previous episode.

**Baselines:** We implement the MTL and CL baselines discussed in Section 2.3: (1) For MTL, each task is randomly sampled. (2) For the curriculum transfer learning (briefly, CL), we start from the easiest task \( T_M \) and gradually move to the main task \( T_{\text{main}} \). For \( \text{wait-} k \), we implement another variant \( \text{wait-} k^* \), where we train \( M \) baseline models on different \( \text{wait-} m \) tasks \( (1 \leq m \leq M) \), and pick the best model according to the validation performance on \( \text{wait-} k \) task. \( \text{wait-} k^* \) is expected to bring additional improvements as pointed out by Ma et al. (2019). After that, we compare with several adaptive methods, including Wait-if-Worse (WIW), Wait-if-Diff (WID), MILk, MMA-IL and MMA-H (refer to Section 3.2 for a brief introduction). Finally, we combine our method with Zheng et al. (2020a). We leave the training details of all algorithms (optimizer, hyperparameter, etc) in Appendix C.2, and the details of baselines in Appendix C.3.

**Evaluation:** We use BLEU to measure the translation quality, and use Average Proportion (AP) and Average Lagging (AL) to evaluate the translation latency. AP measures the average proportion of source symbols required for translation, and AL measures the average number of delayed words (see Appendix A.1. for details). Following the common practice (Ma et al., 2019; 2020), we show the BLEU-AP and BLEU-AL curves to demonstrate the tradeoff between quality and latency. For IWSLT’14 En→De and IWSLT’15 En→Vi, we use \texttt{multi-bleu.pl} to evaluate BLEU scores; for IWSLT’17 En→Zh and WMT’15 En→De, we use \texttt{sacreBLEU} to evaluate the detokenized BLEU scores.

### 3.4. Results and Analysis

We first compare our method with MTL, CL and \( \text{wait-} k^* \) on IWSLT datasets. The BLEU-latency curves are shown in Figure 2, and the BLEU scores of En→Vi are reported in Table 1. For the \( \text{wait-} k^* \), we also report the optimal training task (i.e., \( k^* \)) for each main task \( \text{wait-} k \). BLEU scores of all language pairs are left in Appendix D. Experiments on more heuristic baselines are in Appendix E.2.

![Figure 2: Translation quality against latency metrics (AP and AL) on IWSLT tasks.](image)

| \( k \) | \( \text{wait-} k \) | \( \text{wait-} k^*/k^* \) | CL | MTL | Ours |
|---|---|---|---|---|---|
| 1 | 25.14 | 26.14/5 | 26.01 | 26.12 | 27.03 |
| 3 | 27.17 | 28.25/5 | 26.37 | 28.54 | 29.01 |
| 5 | 28.29 | 28.44/9 | 27.97 | 28.61 | 28.91 |
| 7 | 28.31 | 28.38/13 | 28.31 | 28.77 | 29.17 |
| 9 | 28.39 | 28.39/9 | 28.31 | 28.70 | 29.06 |

Table 1: BLEU scores on IWSLT En→Vi task.
We have the following observations:

1. Generally, our method consistently performed the best across different translation tasks in terms of both translation quality and controllable latency. As shown in Table 1, our method achieves the highest BLEU scores among all baselines. In Figure 2, the curve for our method (i.e., the red one) is on the top in most cases, which indicates that given specific latency (e.g., AP or AL), we can achieve the best translation quality. The results of significance tests are left in Appendix D.

2. MTL and CL can outperform the vanilla baseline, which demonstrates the effectiveness of leveraging the temporally correlated tasks. However, the improvements are not consistent, and it is hard to tell which baseline is better. CL slightly outperforms MTL on En→De. However, on En→Zh, CL performs better at lower latency while MTL performs better at higher latency. In comparison, the improvement brought by our method is much more consistent.

3. Wait-\(k^*\) also outperforms wait-\(k\). Specifically, we notice that the optimal training \(k^*\) is always larger than \(k\) for the main task. This is consistent with the observation in Ma et al. (2019). However, compared with CL and MTL, wait-\(k^*\) does not have a consistent advantage. This shows that the improvements of MTL, CL and our method is not due to the existence of some “best” task in \(T\), and further demonstrates the importance of adaptively using all auxiliary tasks.

The results on WMT'15 En→De, whose training corpus is larger, are shown in Figure 3. Wait-\(k^*\), MTL and CL do not bring much improvement compared to vanilla wait-\(k\). Our method consistently outperforms all baselines, which demonstrates the effectiveness of our method on large datasets. We further evaluate them on WMT'14 and WMT'16 test sets and obtain similar conclusions (see Appendix D for details).

Appendix D. When AL ≥ 5.0, our method outperforms all baseline models, and when AL < 5.0, our method performs slightly worse than MMA-IL and MMA-H. A possible reason is that our method does not explicitly reduce the latency, but focuses on improving performance under given latency constraints.

We further compare and combine our method with Zheng et al. (2020a). We conduct experiments on two variants of Zheng et al. (2020a), where the wait-\(m\) models are obtained through vanilla wait-\(k\) (denoted by “Zheng et al.”) and our strategy respectively (denoted by “Zheng et al. + Ours”). The BLEU-AL curves are shown in Figure 4(b), and the BLEU-AP curves are in Appendix D. We can see that: (1) our method catches up with Zheng et al. (2020a), which is built upon 10 models in total (wait-1, 2, · · · , 10); (2) after combining our approach with Zheng et al. (2020a), the performance can be further boosted, which shows that our method is complementary to adaptive inference strategies like Zheng et al. (2020a).

Computation overhead: To evaluate the additional computational overhead brought by our method, we compare the training speed of standard wait-\(k\) and our method on wait-3 (measured by the number of batches per second). Results on IWSLT datasets are summarized in Table 2. Our method requires 20% ~ 30% additional training time, which is acceptable considering the performance improvements. The major overhead comes from computing the training loss by wait-\(k\). To verify that, we record the training speed of our method without the second and third input features of \(\varphi\), i.e., the training loss over data \((x, y)\) evaluated on wait-\(k\), and the average of historical training losses (denoted by “Ours w/o feature (2,3)”). Without these two features, the training speed of our method is close to wait-\(k\).

Strategy analysis: In Figure 5, we visualize the distribution of wait-\(m\) tasks obtained by the scheduler for two main tasks, wait-3 and wait-9 on IWSLT En→Zh dataset. We show the frequency of each wait-\(m\) task sampled by the scheduler \(\varphi\) at the 0th, 1st, 5th, 10th and 40th episode.

Figure 4: BLEU-AL comparison between our method and baselines on En→Vi.

(a) Comparison with several adaptive methods.
(b) Comparison and combination with Zheng et al. (2020a).
We observed that the scheduler uniformly samples different tasks at first, and then the strategies converge within 10 episodes. After convergence, the scheduler mainly samples several specific tasks, i.e., \( m = 5, 9, 12 \) for \( \text{wait-3} \), and \( m = 5, 12 \) for \( \text{wait-9} \). The task that both schedulers prefer most is \( m = 12 \), which is close to the optimal training task \( \text{wait-9} \) \((k^* = 11)\) for both \( \text{wait-3} \) and \( \text{wait-9} \). This demonstrates that the scheduler can learn which task is more beneficial to the main task. However, it is worth noting that the scheduler also samples other tasks, which shows the importance of training with multiple tasks instead of one single optimal task. For example, the scheduler for \( \text{wait-9} \) samples both \( \text{wait-5} \) and \( \text{wait-9} \) with a probability of about 0.1.

4. Application to Stock Trend Forecasting

4.1. Task Description

Stock trend forecasting is a core problem in stock market investment. Following the common practice, in this task, \( X \) represents the historical transactions data including both prices and trading volumes, and \( Y \) denotes the stock price movement in future days.

At the \( t \)-th day, a specific stock can be represented by a 5-dimension feature vector \( x_t \) including the opening price, closing price (denoted as \( p_t \)), the highest price, the lowest price and the trading volume. The task \( T_k \in T \) is to forecast the stock price rise percent of the next \( k \)-th day, i.e., \( y_t = \frac{p_{t+k} - p_t}{p_t} - 1 \). This task lies in the second type of classes as introduced in Section 2.1. In stock forecasting, we usually make predictions based on a window of historical inputs of length \( L \), i.e., \((x_{t-L+1}, x_{t-L+2}, \cdots, x_t)\). We explore three different main tasks in this work: forecasting the stock rise trend of the next 1st, 2nd and 3rd days (i.e., \( T_1, T_2 \) and \( T_3 \)). As mentioned by Tang et al. (2020), all the above three tasks are important because investors tend to invest in stocks with rising price trends in a continuous period, rather than caring the next trading day only.

4.2. Background

Traditional methods for stock trend forecasting are based on time-series analysis models, such as the Auto-regressive Integrated Moving Average (ARMA) and Kalman Filters (Yan & Guosheng, 2015). With the development of deep learning, applying neural network to stock forecasting becomes a new trend due to its better performance on noisy data. GRU (Chung et al., 2014) is one of the most representative deep neural networks in stock trend forecasting (Hu et al., 2018). By utilizing the reset gate and update gate, GRU can adaptively choose the information to be kept or dropped, which makes it relatively robust to the diverse and noisy sequential data in the stock market. Other types of recurrent neural networks are also leveraged such as LSTM, SFM (Zhang et al., 2017b), ALSTM (Qin et al., 2017b), etc. Recent works start to use graph neural networks (e.g. GAT (Veličković et al., 2017)) to model different stocks so that the information can be propagated along with the pre-defined relations (Feng et al., 2019; Kim et al., 2019). In addition to neural networks, many machine learning meth-

| Task     | \( \text{wait-k} \) | Ours     | Ours w/o feature (2,3) |
|----------|-----------------|----------|------------------------|
| En→De   | 5.3 (4.0 (-23%)) | 5.2 (5.1 (-2%)) |
| En→Vi   | 1.5 (1.1 (-27%)) | 1.4 (1.5 (-7%)) |
| En→Zh   | 2.5 (1.8 (-28%)) | 2.4 (2.4 (-4%)) |

Table 2: Comparison of training speed (batch / sec) between \( \text{wait-k} \) and our methods.
ods have been successfully applied to forecast stock future trends. A particularly powerful branch is the tree-based approach, such as LightGBM (Ke et al., 2017) and Random Forest. They have outstanding performance and certain interpretability, so they are widely used in stock market investment (Khaidem et al., 2016; Tan et al., 2019).

4.3. Settings

We conduct experiments on individual stocks in the Chinese A-share market. We explore three groups of temporally correlated tasks: \( T_3 = \{T_1, T_2, T_3\} \), \( T_5 = \{T_1, T_2, \cdots, T_5\} \) and \( T_{10} = \{T_1, T_2, \cdots, T_{10}\} \).

**Dataset**: We use the historical transaction data for 300 stocks on CSI300 (CSI300, 2008) from 01/01/2008 to 08/01/2020. We split the data into training (01/01/2008-12/31/2013), validation (01/01/2014-12/31/2015), and test sets (01/01/2016-08/01/2020) based on the transaction time. All the data is provided by Yang et al. (2020).

**Models**: The forecasting model \( f \) is built on top of a 2-layer GRU with hidden dimension 32. The length of the input sequence (i.e., the \( L \) in Section 4.1) is 60. The scheduler \( \varphi \) is a single-layer feed-forward network with ReLU activation. The hidden size of \( \varphi \) is 32.

**Input features of \( \varphi \)**: The features consist of four parts: (1) the data \((x, y) \in D_t\) itself; (2) the training loss of the previous iteration; (3) the forecasting results of the previous iteration; (4) the labels of each task in \( T \).

**Baselines**: Similar to Section 3.3, we implement MTL and CL as baselines by using temporally correlated tasks. In CL, we start from the easiest task \( T_1 \), and then gradually move to the most difficult one. Besides, we implement different models for stock forecasting for comparison, including simple feed-forward networks (denoted by MLP), lightGBM (briefly, LGB) (Ke et al., 2017) and GAT (Veličković et al., 2017; Feng et al., 2019). Note that for GAT, we do not leverage the specific relation between stocks.

**Evaluation**: We use rank correlation coefficient (Zhang et al., 2020) (briefly, RankIC) and the mean square error (briefly, MSE) to evaluate the forecasting results. RankIC can be regarded as a correlation between the prediction and the groundtruth results (the larger, the better). MSE measures the gap between prediction results and the groundtruth results (the smaller, the better). Due to space limitation, we put the evaluation results using ICIR (a measurement that takes stability into consideration) in Appendix F.

4.4. Results and Analysis

The results of stock trend forecasting are reported in Table 3. We have the following observations:

1. With different sets of temporally correlated auxiliary tasks, i.e., \( T_3, T_5 \) and \( T_{10} \), our method significantly outperforms MTL and CL on most settings, which demonstrates the effectiveness of leveraging an adaptive scheduler.

2. Using a larger temporally correlated task set does not always bring improvements. Taking task \( T_1 \) as an example, our method achieves the best performance when using 5 temporally correlated tasks, while using 10 hurts the performance. The reason is that more tasks will introduce additional noise to the training.

3. There are more advanced methods than GRU like GAT, leveraging temporally correlated tasks can achieve superior performance than the strong models. Currently, our model is based on GRU, and we will combine our method with GAT and lightGBM in the future for more improvements.

5. Conclusions and Future Work

In this work, we formulated and studied the problem of temporally correlated task scheduling, which can cover many applications including sequence processing with latency constraints (e.g., simultaneous machine translation) and sequence future prediction (e.g. stock trend forecasting). Experiments on four translation tasks and one stock prediction task demonstrate the effectiveness of our approach.

For future work, we will apply our method to more applications like action prediction (Kong et al., 2020; Cai et al., 2019), streaming speech recognition, weather forecasting, game AI (Li et al., 2020; Vinyals et al., 2019), etc. We will also design better methods for the problem. Another interesting direction is to theoretically understand the problem and analyze our method.

| Methods    | Task-1  | Task-2  | Task-3  |
|------------|---------|---------|---------|
| GRU        | 0.049 / 1.903 | 0.018 / 1.972 | 0.014 / 1.989 |
| MLP        | 0.023 / 1.961 | 0.022 / 1.962 | 0.015 / 1.978 |
| LGB        | 0.038 / 1.883 | 0.023 / 1.952 | 0.007 / 1.987 |
| GAT        | 0.052 / 1.898 | 0.024 / 1.954 | 0.015 / 1.973 |
| MTL (10)   | 0.061 / 1.862 | 0.023 / 1.942 | 0.012 / 1.956 |
| CL (T5)    | 0.051 / 1.880 | 0.028 / 1.941 | 0.016 / 1.962 |
| Ours (T5)  | 0.071 / 1.851 | 0.030 / 1.939 | 0.017 / 1.963 |
| MTL (10)   | 0.057 / 1.875 | 0.021 / 1.939 | 0.017 / 1.959 |
| CL (T10)   | 0.056 / 1.877 | 0.028 / 1.942 | 0.015 / 1.962 |
| Ours (T10) | 0.075 / 1.849 | 0.032 / 1.939 | 0.021 / 1.955 |
| MTL (T3)   | 0.052 / 1.882 | 0.020 / 1.947 | 0.019 / 1.952 |
| CL (T3)    | 0.051 / 1.882 | 0.028 / 1.950 | 0.016 / 1.961 |
| Ours (T3)  | 0.067 / 1.867 | 0.030 / 1.960 | 0.022 / 1.942 |
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A. Mathematical definitions

A.1. Latency metrics definitions

Given the input sentence $x$ and the output sentence $y$, let $L_x$ and $L_y$ denote the length of $x$ and $y$ respectively. Define a function $g(t)$ of decoding step $t$, which denotes the number of source tokens processed by the encoder when deciding the target token $y_t$. For wait-$k$ strategy, $g(t) = \min\{t + k - 1, L_x\}$. The definitions of Average Proportion (AP) and Average Lagging (AL) are in Eqn.(3) and Eqn.(4) respectively.

\[
AP_g(x, y) = \frac{1}{|x||y|} \sum_{t=1}^{|y|} g(t); \\
AL_g(x, y) = \frac{1}{\tau_g(|x|)} \sum_{t=1}^{\tau_g(|x|)} \left( g(t) - \frac{t-1}{|y|/|x|} \right),
\]

where $\tau_g(|x|) = \min\{t \mid g(t) = |x|\}$.

We use the scripts provided by Ma et al. (2019) to calculate AP and AL scores.

A.2. Mathematical formulation of curriculum transfer learning

For a group of temporally correlated tasks $\mathcal{T} = \{T_1, T_2, \cdots, T_M\}$, suppose $\mathcal{T}$ is ordered by task difficulty. That is, $T_M$ is the easiest task, followed by $T_{M-1}, T_{M-2}$, etc, and $T_1$ is the hardest task. In the curriculum transfer learning (briefly, CL) baseline, we gradually change the training task $T_m$ from the easiest task $T_M$ to the main task, supposedly, $T_k$. The mathematical formulations are shown as follows:

\[
m = M - \left\lfloor \frac{t-1}{t_{\text{max}}} (M - k + 1) \right\rfloor
\]

where $t$ denotes the current update number ($t = 1, 2, ..., t_{\text{max}}$), and $t_{\text{max}}$ denotes the total update number.

B. Model architecture

Following Ma et al. (2019), our model for simultaneous NMT is based on Transformer model (Vaswani et al., 2017). The model includes an encoder and a decoder, which are used for incrementally processing the source and target sentences respectively. Both the encoder and decoder are stacked of $L$ blocks.

In Ma et al. (2019), every time a new token is read, the encoder needs to re-encode the entire sentence, which is computationally expensive. To improve the efficiency, we adopt incremental encoding, so that after reading a new token, we only encode the new token rather than updating the representations of the whole sentence. The details are as follows:

1) Incremental encoding: Let $h^l_i$ denote the output of the $t$-th position from block $l$. For ease of reference, let $H_{\leq t}^l$ denote $\{h^l_1, h^l_2, \cdots, h^l_t\}$, and let $h^0_l$ denote the embeddings of the $t$-th token. An attention model $\text{attn}(q, K, V)$, takes a query $q \in \mathbb{R}^d$, a set of keys $K$ and values $V$ as inputs. $K$ and $V$ are of equal size, $q \in \mathbb{R}^d$ where $d \in \mathbb{Z}_+$ is the dimension, $k_i \in \mathbb{R}^d$ and $v_i \in \mathbb{R}^d$ are the $i$-th key and value. $\text{attn}$ is defined as follows:

\[
\text{attn}(q, K, V) = \sum_{i=1}^{[K]} \alpha_i W_v v_i, \quad \alpha_i = \frac{\exp((W_q q)^\top (W_k k_i))}{Z}, \quad Z = \sum_{i=1}^{[K]} \exp((W_q q)^\top (W_k k_i)),
\]

where $W$’s are the parameters to be optimized. In the encoder side, $h^l_t$ is obtained in a unidirectional way: $h^l_t = \text{attn}(h^l_{t-1}, H_{\leq t-1}^l)$. That is, the model can only attend to the previously generated hidden representations, and the computation complexity is $O(L_2^2)$. In comparison, (Ma et al., 2019) still leverages bidirectional attention, whose computation complexity is $O(L_3^2)$. We find that unidirectional attention is much more efficient than bidirectional attention without much accuracy drop (see Appendix B for details).

2) Incremental decoding: Since we use wait-$k$ strategy, the decoding starts before reading all inputs. At the $t$-th decoding step, the decoder can only read $x_{\leq t+k-1}$. When $t \leq L_x - k$, the decoder greedily generates one token at each step, i.e., the
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token is $y_t = \arg \max_{w \in V} P(w \mid y_{\leq t-1}; H_{\leq t+k-1}^L)$, where $V$ is the vocabulary of the target language. When $t > L_x - k$, the model has read the full input sentence and can generate words using beam search (Ma et al., 2019).

We compare the performance of original Ma et al. (2019) and our modified model on IWSLT’14 En→De dataset, and the results are in Figure 6. On IWSLT’14, we observe that the performance of our model slightly drops compared to Ma et al. (2019). However, the computational cost of Ma et al. (2019) is much larger than our modified model. For example, the inference speed of our wait-9 model is 57.39 sentences / second, while the inference speed of Ma et al. (2019) is 6.48 sentences / second.

![Figure 6: Ablation study of different model architectures on IWSLT’14 En→De dataset and WMT’15 En→De dataset.](image)

C. More detailed settings about experiments

C.1. Detailed introduction of the datasets

For IWSLT’14 En→De, following (Edunov et al., 2018), we lowercase all words, tokenize them and apply BPE with 10$k$ merge operations jointly to the source and target sequences. We split 7$k$ sentences from the training corpus for validation and the remaining 160$k$ sequences are left as the training set. The test set is the concatenation of tst2010, tst2011, tst2012, dev2010 and dev2012, which consists of 6750 sentences.

For IWSLT’15 En→Vi, following (Ma et al., 2020), we tokenize the data and replace words with frequency less than 5 by <unk>\(^1\). We use tst2012 as the validation set and tst2013 as the test set. The training, validation and test sets contain 133$k$, 1268 and 1553 sentences respectively.

For IWSLT’17 En→Zh, we tokenize the data and apply BPE with 10$k$ merge operations independently to the source and target sequences\(^2\). We use the concatenation of tst2013, tst2014 and tst2015 as the validation set and use tst2017 as the test set. The training, validation and test sets contain 235$k$, 3874 and 1459 sentences respectively. For WMT’15 En→De, we follow the setting in (Ma et al., 2019; Arivazhagan et al., 2019). We tokenize the data, apply BPE with 32$k$ merge operations jointly to the source and target sentences, and get a training corpus with 4.5M sentences. We use newstest2013 as the validation set and use newstest2015 as the test set.

C.2. Detailed training strategy

For the translation model, we use Adam (Kingma & Ba, 2015) optimizer with initial learning rate $5 \times 10^{-4}$ and inverse_sqrt scheduler (see Section 5.3 of (Vaswani et al., 2017) for details). The batch size and the number of GPUs of IWSLT En→De, En→Vi, En→Zh and WMT’15 En→De are 4096 × 1GPU, 16000 × 1GPU, 4000 × 1GPU and 3584 × 8 × 16GPU respectively. For IWSLT tasks, the learning rate $\eta$ is grid searched from $\{5 \times 10^{-4}, 5 \times 10^{-5}, 5 \times 10^{-6}, 5 \times 10^{-7}\}$ with vanilla SGD optimizer, and the internal update iteration $S$ is grid searched from $\{S_e, S_e, 2S_e\}$.

\(^1\)The data is downloaded from https://nlp.stanford.edu/projects/nmt/, which has been tokenized already.

\(^2\)The Chinese sentences are tokenized using Jieba (https://github.com/fxsjy/jieba).
where \( S \) is the number of updates in an epoch of the translation model training. For WMT’15 En→De, due to resource limitation, we do not train the translation model from scratch. The translation model is warm started from pretrained \( wait-k \) model, the learning rate is set as \( 5 \times 10^{-5} \), and the internal update iteration \( S \) is 16.

**C.3. Detailed baseline implementation**

In this section, we introduce how we reproduce baseline models and get the results on En→Vi task.

For MILk (Arivazhagan et al., 2019) and MMA (Ma et al., 2020), we do not reproduce the results, but directly use the results reported in Ma et al. (2020). Note that the results for MILk is reproduced by Ma et al. (2020).

For WIW and WID (Cho & Esipova, 2016), we pre-train a standard translation model, using the exact same architecture and training hyperparameters as our method and in (Ma et al., 2020). For fair comparison, we adopt bi-directional attention.

For Zheng et al. (2020a), we use the pre-trained \( wait-k \) model and the model obtained through our results \((k = 1, 2, 3, \ldots, 10)\). We use only single model rather than ensemble. As in Zheng et al. (2020a), the thresholds of different \( k \) values are obtained in this way: \( \rho_i = \rho_1 - (i - 1) \times (\rho_1 - \rho_{10})/9 \), where we test with \( \rho_1 \in \{0.2, 0.4, 0.6, 0.8\} \), \( \rho_{10} = 0 \); and \( \rho_1 = 1 \), \( \rho_{10} \in \{0, 0.2, 0.4, 0.6, 0.8\} \).

**D. Supplemental results**

In this section, we report the specific BLEU scores and some additional results. The BLEU scores for IWSLT tasks and WMT’15 En→De task are reported in Table 4 and Table 5 respectively. We further evaluate the baselines and our methods on WMT’14 and WMT’18 test sets, and report the BLEU-latency curves in Figure 8. The BLEU-AL curves of our methods and baselines on IWSLT’15 En→Vi are reported in Figure 7(a), the BLEU-AL curves of our method and Zheng et al. (2020a) are in Figure 7(b).

For significance tests, we compare our method with MTL on all 20 translation tasks (En→{Vi, Zh} tasks and two En→De tasks, where each task is associated with 5 settings, i.e. \( wait-1,3,5,7,9 \)), and find that our method significantly outperforms MTL on 16 tasks with \( p < 0.05 \), where 11 out of them are with \( p < 0.01 \).

| Task      | \( wait-k \) | \( wait-k^* \) / best \( k^* \) | CL      | MTL     | Ours     |
|-----------|--------------|----------------------------------|---------|---------|---------|
| En→De \((k = 1)\) | 16.75        | 19.11 / 9                        | 18.23   | 18.53   | 19.10   |
| En→De \((k = 3)\) | 22.79        | 23.36 / 13                       | 23.41   | 23.50   | 24.12   |
| En→De \((k = 5)\) | 25.34        | 25.76 / 11                       | 25.88   | 25.84   | 26.54   |
| En→De \((k = 7)\) | 26.74        | 26.87 / 9                        | 26.85   | 26.88   | 27.37   |
| En→De \((k = 9)\) | 27.25        | 27.54 / 11                       | 27.48   | 27.07   | 27.87   |
| En→Vi \((k = 1)\) | 25.14        | 26.14 / 5                        | 26.01   | 26.12   | 27.03   |
| En→Vi \((k = 3)\) | 27.17        | 28.25 / 5                        | 26.37   | 28.54   | 29.01   |
| En→Vi \((k = 5)\) | 28.29        | 28.44 / 9                        | 27.97   | 28.61   | 28.91   |
| En→Vi \((k = 7)\) | 28.31        | 28.38 / 13                       | 28.31   | 28.77   | 29.17   |
| En→Vi \((k = 9)\) | 28.39        | 28.39 / 9                        | 28.31   | 28.70   | 29.06   |
| En→Zh \((k = 1)\) | 14.24        | 19.34 / 9                        | 17.26   | 18.02   | 19.21   |
| En→Zh \((k = 3)\) | 19.90        | 21.66 / 11                       | 21.64   | 21.36   | 22.18   |
| En→Zh \((k = 5)\) | 21.45        | 23.57 / 11                       | 23.62   | 22.59   | 23.70   |
| En→Zh \((k = 7)\) | 23.23        | 24.95 / 11                       | 24.32   | 23.15   | 24.35   |
| En→Zh \((k = 9)\) | 23.93        | 24.83 / 11                       | 24.55   | 23.55   | 24.78   |

Table 4: BLEU scores on IWSLT simultaneous NMT tasks.
(a) Comparison of our method, WIW, WID, MILk, MMA-IL and MMA-H.

(b) Comparison and combination of our method and Zheng et al. (2020a).

Figure 7: BLEU-AP comparison between our method and baselines on En→Vi.

(a) BLEU-AP, WMT’14 En→De
(b) BLEU-AP, WMT’16 En→De
(c) BLEU-AL, WMT’14 En→De
(d) BLEU-AL, WMT’16 En→De

Figure 8: Translation quality against latency metrics (AP and AL) on WMT’14 and 16 English→German test sets.
E. Additional ablations and analysis on simultaneous translation

E.1. Feature selection

To emphasize the importance of the selected features in Section 3.3 in the main content, we provide four groups of ablation study, where in each group some specific features are excluded: (i) source and target sentence lengths; (ii) current training loss and average historical training loss; (iii) current validation loss and average historical validation loss; (iv) training step. We work on IWSLT’14 En→De task and study the effect to wait-3, 5, 7.

The results are shown in Table 6. We report the BLEU scores only, since the latency metrics (AP and AL) are not significantly influenced. Removing any feature causes performance drop, indicating that they all contribute to the decision making. Specifically, network status information including validation performance (feature iii) and training stage (feature iv) is more important than input data information including sequence length (feature i) and data difficulty (feature ii).

| k   | wait-k | wait-k*/best k* | CL  | MTL  | Ours |
|-----|--------|-----------------|-----|------|------|
| 1   | 17.07  | 19.83 / 9       | 19.41 | 17.59 | 18.63 |
| 3   | 22.86  | 23.14 / 7       | 22.51 | 22.76 | 23.98 |
| 5   | 25.52  | 26.09 / 7       | 25.51 | 25.66 | 26.77 |
| 7   | 27.32  | 27.50 / 9       | 26.80 | 26.91 | 27.92 |
| 9   | 28.05  | 28.05 / 9       | 28.20 | 27.82 | 28.67 |

Table 6: Ablation study for feature selection on IWSLT’14 En→De dataset.

E.2. More heuristic baselines

In this section, we conduct ablation studies on two more heuristic baselines to demonstrate the effectiveness of our method.

1. **Randomly selecting k in a window around k**: We implement another baseline which is a combination of wait-k* and MTL. After obtaining k*, instead of sampling wait-m on all possible \( \{1, 2, \cdots, M\} \), we sample on a smaller region around k*. We conduct experiments on IWSLT En→De and the results are in Figure 9. We can see that this variant achieves similar results with wait-k*, but is not as good as our method. This shows the importance of using an adaptive controller to guide the training.

2. **A variant of CL**: Considering that the curriculum transfer learning is related to curriculum learning, we implement self-paced learning (SPL) for wait-k, a CL method based on loss function: within each minibatch, we remove the \( \tau \% \) sentences with the largest loss, where \( \tau \) is gradually decreased from 40 to 0. On IWSLT En→De, when \( k = 3 \), the BLEU/AL/AP for SPL are 22.87/0.66/3.47, which are worse than conventional CL (23.41/0.66/3.48).

3. **An annealing strategy**: Inspired by the fact that wait-k* outperforms wait-k, we design a baseline where we randomly sample the waiting threshold m from a distribution \( p_t(m) \) at each training step t. The distribution \( p_t(m) \) linearly anneals from a uniform distribution to a distribution which prefers larger m. We expect a single annealing strategy can train reasonably good models for different inference-time k values. Suppose the minimal m value is \( m_{\text{min}} \), the maximal m value is \( m_{\text{max}} \). \( m_{\text{min}} \) and \( m_{\text{max}} \) are two integers and m \( \in \{m_{\text{min}}, m_{\text{min}} + 1, \cdots, m_{\text{max}}\} \). The total training step is denoted as \( t_{\text{max}} \).
Figure 9: Randomly selecting $k$ in a window around $k^\ast$.

$p_t(m)$ is mathematically defined as follows:

$$p_t(m) = (1 - \frac{t}{t_{\text{max}}}) \cdot p_{\text{init}}(m) + \frac{t}{t_{\text{max}}} \cdot p_{\text{final}}(m),$$

$$p_{\text{init}}(m) = \frac{1}{m_{\text{max}} - m_{\text{min}} + 1}, \quad p_{\text{final}}(m) = \frac{m}{\sum_{i=m_{\text{min}}}^{m_{\text{max}}} i}.$$  \hfill (7)

The results on IWSLT’15 En→Vi are shown in Figure 10, which shows this baseline brings limited improvement compared to wait-$k$. A possible reason is that this baseline cannot guarantee the best “annealing” strategy for each separate $k$, while our method can adaptively find the optimal strategy. Besides, as shown in Figure 5 in the main content, the learned strategies for different wait-$k$ inference are pretty different.

F. More details about stock trend forecasting

F.1. Detailed introduction of the datasets

For the Chinese A-share market dataset used in stock trend forecasting tasks, all the price and volume data are loaded from Qlib (Yang et al., 2020). In this paper, only the stocks in CSI300 are included in the experiments. CSI300 consists of the 300 largest and most liquid A-share stocks, that can reflect the overall performance of China A-share market.
F.2. Training details

For the stock trend forecasting models, we select the optimal hyper-parameters including learning rate, dropout rate, batch size and optimizer of scheduler and the sequence length $L$ on the validation set. We repeat each experiment by using 5 random seed and report the average scores (RankIC, ICIR and MSE) to get the final result.

F.3. Supplemental results

We report the specific ICIR scores for stock trend forecasting task in Table 7. Comparing with RankIC and MSE, similar phenomenon can be observed: 1) with temporally correlated tasks, our method significantly outperforms MTL and CL on most settings; 2) using a larger temporally correlated task set does not always bring improvements; 3) our method performs better than some strong models like GAT and lightGBM (briefly, LGB).

|        | Task-1 | Task-2 | Task-3 |
|--------|--------|--------|--------|
| GRU    | 0.373  | 0.127  | 0.111  |
| MLP    | 0.175  | 0.164  | 0.116  |
| LGB    | 0.297  | 0.180  | 0.070  |
| GAT    | 0.389  | 0.133  | 0.113  |
| MTL    |        |        |        |
| 3tasks | 0.467  | 0.179  | 0.083  |
| 5tasks | 0.444  | 0.146  | 0.115  |
| 10tasks| 0.403  | 0.134  | 0.135  |
| CL     |        |        |        |
| 3tasks | 0.397  | 0.198  | 0.112  |
| 5tasks | 0.419  | 0.200  | 0.110  |
| 10tasks| 0.393  | 0.200  | 0.117  |
| Ours   |        |        |        |
| 3tasks | 0.559  | 0.228  | 0.126  |
| 5tasks | 0.583  | 0.203  | 0.117  |
| 10tasks| 0.532  | 0.222  | 0.160  |

Table 7: ICIR scores. The first four rows are the results of various model architectures without leveraging temporally correlated tasks. The following rows are the results with different algorithms and different task sets.