Optimizing PEMFC model parameters using ant lion optimizer and dragonfly algorithm: a comparative study

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ABSTRACT
This paper introduced two optimization algorithms which are Ant Lion Optimizer (ALO) and Dragonfly Algorithm (DA) for extracting the Proton Exchange Membrane Fuel Cell (PEMFC) polarization curve parameters. The results produced by both algorithms are being compared to observe their performance. As a results, the ALO shows great performance compared to DA. Furthermore, these results also being compared with the results of the other reported metaheuristics algorithms. The ALO and DA presented competitive results.

Keywords:
Optimizing PEMFC parameters
PEMFC model
Ant lion optimizer
Dragonfly algorithm
Metaheuristic algorithm

1. INTRODUCTION

Currently, the attention of using the metaheuristic algorithms in solving engineering problems had increased significantly. These due to they are derivative-free, impose no restrictions on the problem formulation, and can be easily adapted for various real world problems [1–7]. Proton Exchange Membrane Fuel Cell (PEMFC) is a hydrogen based fuel cell. A hydrogen-rich fuel is injected to the anode, and an oxidant which usually use pure oxygen or air is fed through the cathode [8]. It mainly used for portable and mobile application due to it compactness, small in size, low weight with high power density and pollutants free operation [8, 9]. Obtaining accurate parameters from actual PEMFC directly is important for modelling purpose but difficult due to its complexity. In the past decades, some existing metaheuristic algorithms, such as Differential Evolution Algorithm (DE) [10–12], Artificial Immune System [13], Artificial Bee Colony [14, 15], Particle Swarm Optimization (PSO) [16, 17], Genetic Algorithm (GA) [18, 19], Backtracking Search Algorithm (BSA) [20] and Bird Mating Optimizer (BMO) [21], have been applied in identifying the electrochemical-based model parameters of PEMFC.

Each metaheuristic algorithms have their own attributes and strategies to reach the global optima with minimum number of iteration without entrapping at local optima. This can be achieved with a good balancing between the exploration and exploitation processes. However, according to No Free Lunch Theorem for optimization [22], a single method cannot fit to every optimization problems. This leads to the application of new algorithm in solving the optimization problem. In this paper, two optimization algorithms, proposed by Mirjalili, the Ant Lion Optimizer algorithm (ALO) [23] and Dragonfly Algorithm (DA) [24] were exploited to extract the PEMFC electrochemical-based model parameters. The ALO
is simulating the hunting mechanism of ant lions, meanwhile the DA simulate the static and dynamic swarming behaviors of dragonflies in nature. The performance of both algorithms in obtaining the parameters of PEMFC stack are compared and analyzed with subsequent discussions. The Ballard Mark V PEMFC (BM5), as being reported and used in many literatures [10, 20, 21, 25, 26], is used as the test bench. Furthermore, the best results is then being compared with other algorithms reported in the literature to observe their real performance.

The remainder of this paper is organized as follows: Mathematical Modelling of Polarization Curve Section which represent the PEMFC mathematical model using electrochemical model and Problem Formulation Section describe the objective function selected for optimization process. In Optimization Algorithm Section, the ALO and DA are briefly described. In Optimization Results Section, the performance of both algorithms in determining the PEMFC model parameters are observed and discussed. Then, the best results are compared with other optimization approaches. Finally, the conclusion and future research are drawn in Conclusions Section.

2. MATHEMATICAL MODELLING OF POLARIZATION CURVE

This paper adopted the basic model from [27], where three (3) different kinds of voltage drops are taken for the model development. The output voltage for a PEMFC cell stack \( V_{cell} \) is calculated as [28]:

\[
V_{cell} = N_s \times \left( E_{Nernst} - V_{act} - V_{con} - V_{ohmic} \right)
\]  

(1)

where \( N_s \) is the number of cell in a stack, \( E_{Nernst} \) is the reversible fuel cell voltage. Meanwhile, the \( V_{act} \), \( V_{con} \), and \( V_{ohmic} \) are the voltages drop due to activation losses at the lower currents, concentration voltage losses at higher currents, and the ohmic losses at the intermediate currents, respectively. The \( E_{Nernst} \) can be obtained as follows:

\[
E_{Nernst} = 1.229 - 0.85 \times 10^{-3}(T - 298.15) + 4.31 \times 10^{-3} \times (\ln(P_{H_2}) + 0.5 \ln(P_{O_2}))
\]  

(2)

where \( P_{H_2} \) and \( P_{O_2} \) are correspondingly partial pressures of hydrogen and oxygen in atm while \( T \) represents the cell temperature in Kelvin.

The \( V_{act} \) is defined as [10]:

\[
V_{act} = \left[ \xi_1 + \xi_2 T + \xi_3 T \ln(C_{O_2}) + \xi_4 T \ln(i) \right]
\]  

(3)

where \( \xi_1, \xi_2, \xi_3 \) and \( \xi_4 \) are the semi-empirical coefficients and \( i \) is the cell current. \( C_{O_2} \) is the oxygen concentration (mol cm\(^{-3}\)) in the cathode interface and defined as:

\[
C_{O_2} = \frac{P_{O_2}}{5.08 \times 10^6 \times e^{(-498/T)}}
\]  

(4)

The \( V_{ohmic} \) can be calculated by:

\[
V_{ohmic} = i \times (R_M + R_C)
\]  

(5)

where \( R_M \) and \( R_C \) are the equivalent membrane resistance (\( \Omega \) cm\(^2\)) and the contact resistance (\( \Omega \) cm\(^2\)) between electrodes and membrane as well as the electrodes and bipolar plates, respectively [26]. \( R_M \) is defined as:

\[
R_M = \frac{\rho_M \times \ell}{A}
\]  

(6)
where $\rho_M$ is the specific membrane resistivity (Ω cm) and $\ell$ is the membrane thickness (cm) that acts as a cell electrolyte while $A$ is the active cell area (cm²). The $\rho_M$ value can be obtained using as follows:

$$\rho_M = \frac{181.6[1 + 0.03\left(\frac{i}{A}\right) + 0.062\left(\frac{T}{303}\right)^2(i/A)^{1.5}}{\left[\lambda - 0.643 - 3\left(\frac{i}{A}\right)\exp\left[4.18\left(\frac{T - 303}{T}\right)\right]\right]}$$

(7)

where $\lambda$ is an adjustable parameter that related to the water content of the membrane. Finally, the $V_{con}$ is defined as:

$$V_{con} = -b \ln \left(1 - \frac{J + J_n}{J_{max}}\right)$$

(8)

where $b$ is the parametric coefficient, $J$ is the current density (A cm⁻²), $J_{max}$ is the maximum current density (A cm⁻²) and $J_n$ is internal current density due to fuel crossover and internal currents [14]. Most of the time, $J_n$ can be neglected since it value is very small, however, Correa et al. [29] stated that $J_n$ has a considerable effect on the model results especially at lower currents. Therefore, $J_n$ is being considered in the calculation in this paper.

3. PROBLEM FORMULATION

Based on the stated equations in section 2, there are 11 unknown parameters involved in describing the PEMFC operation. These unknown parameters are $\xi_1, \xi_2, \xi_3, A, \ell, R, J_n, J_{max}, b, \rho_M$, and $\lambda$. A performance criterion or an objective function is defined for an optimization purpose. In this work, the mean square error (MSE) between the output voltage of the actual PEMFC stack and the model output voltage are used as the objective function [10]:

$$MSE = \frac{1}{N} \sum_{j=1}^{N} \left(V_{i,m} - V_i\right)^2$$

(9)

where $V_{i,m}$ is the measured output voltage of the actual PEMFC stack, $V_i$ is the model output voltage, and $N$ is the number of the experimental data point.

4. OPTIMIZATION ALGORITHM

In this part, the ALO and DA are being described briefly. Both algorithms were introduced by Mirjalili in 2015. The Ant Lion Optimizer is a heuristic optimization algorithm that mimics the hunting mechanism of antlions in nature. Five main steps of hunting prey such as the random walk of ants, building traps, entrapment of ants in traps, catching preys, and re-building traps are implemented. Figure 1 shows the flowchart of the ALO. Details description of the process can be referred to [23].

The DA was initiated from the static and dynamic swarming behaviors of dragonflies in nature [24]. The exploration and exploitation phases are designed by modeling the social interaction of dragonflies in navigating, searching for foods, and avoiding enemies when swarming in dynamically or statistically [24, 30]. There are five factors involved in determining the individual dragonfly position [24, 30, 31]:

a. The static collision avoidance of the individuals from other individuals in the neighborhood (separation).

b. The velocity matching of individuals to other individuals in the neighborhood (alignment).

c. The tendency of individuals towards the center of the mass of the neighborhood (cohesion).

d. Attracted towards food sources

e. Distracted outward enemies
The flow of the DA execution is summarized in Figure 2. Details explanation of the execution processes can be referred to original paper by Mirjalili [24].

5. RESULTS AND ANALYSIS

A single cell Ballard Mark V PEMFC, extracted from [10] is chosen to evaluate the optimization capability of ALO and DA. Simulation have been done using Intel® Core™ i5 processors with MATLAB version 2017. In this work, there are 11 unknown parameters of PEMFC required to be optimized. The ranges of these parameters are shown in Table 1. Before implement both algorithms in MATLAB software, the adjustable parameters need to be tuned. The setup similar with work done by A.Askarzadeh [20] was adopted; the population size is set to 30 and the maximum number of iteration is equal to 2000. The algorithm is executed 50 times for each fuel cell in order to get the best objective function optimal value.

| Parameter | \( \xi_1 \) | \( \xi_2 \) | \( \xi_3 \) | \( \xi_4 \) | \( \lambda \) | \( R_c (\Omega) \) | \( B (V) \) | \( J_n (mA/cm^2) \) | \( J_{max} (mA/cm^2) \) | \( t (\mu m) \) | \( A (cm^2) \) |
|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| Lower Bound | -1.1997 | 0.001 | 3.60E-05 | -2.60E-04 | 10 | 0.0001 | 0.0136 | 1 | 500 | 20 | 20 |
| Upper Bound | -0.8532 | 0.005 | 9.80E-05 | -9.54E-05 | 24 | 0.0008 | 0.5 | 30 | 1500 | 200 | 100 |

Figure 1. Flowchart of the ant lion optimizer algorithm
Figure 2. Flowchart of the dragonfly algorithm

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Figure 3 display the tabulation of best objective value for 50 runs of a single cell BM5 obtained for ALO and DA. Observing this figure, it is clearly being seen that ALO produced better results (low error generated) compared to DA (45 out of 50). This is proved by calculated mean value. The ALO mean value is 3.2610e-5 which is lower than mean value for DA (4.2924e-5). Examine further, the results produced by ALO are more stable and precise which are closed to each other except for run no 2 and 18 which quite rare and can be neglected. In addition, in order to compare the significance difference between these two algorithms, the nonparametric Wilcoxon rank sum test was used [32]. The significance level is set to 5% (α=0.05). The null hypothesis (h₀) assumes that there is no significant difference between the ALO and DA. However, the obtained p-value (3.9946e-13) is below the significant level, proving that the results of ALO is statistically significant.

The convergence curves of the best objective value for both algorithms are shown in Figure 4. Even though ALO and DA entrapped at local optima for a few times, however, they are able to escape to obtain the global optimum. Moreover, even though the DA converges faster in early iteration, however, the ALO has better adjustment and increase it convergence speed after 200 iterations. This capability leads to the better solution produced by ALO compared to DA. Furthermore, the I-V curves are plotted using the parameters obtained for the best objective function together with the experimental values. Figure 5 shows the I-V curve for BM5. Observing the figure it can been seen that the curve generated using parameters attained by ALO and DA are in good arrangement with the experimental data.

With the intention of further understanding the performance of ALO and DA, the obtained results are compared with the reported results presented in Ref. [10], the same PEMFC model with 11 unknown parameters have been used. In Ref. [10], the parameters identified using Transferred Adaptive Differential Evolution (TRADE), Bird Mating Optimizer (BMO), Backtracking search optimization algorithm (BSA), and Burger's chaotic map (BSABCM-3) are stated. The extracted parameters and their corresponding objective function values for BM5 are displayed in Table 2. Observing the results in Tables 2 clearly reveal that the MSE obtained by both algorithms are smaller compared with other four methods in Ref. [10]. This reveals the better accuracy and the efficiency of the proposed method.
Figure 4. The best objective value convergence curve for Ballard Mark V PEMFC

Figure 5. I-V curve for Ballard Mark V PEMFC
Table 2. Parameters value and operation condition of Ballard Mark V PEMFC stack

| Parameter   | TRADE  | BMO    | BSA    | BSABSM-3  | DA     | ALO   |
|-------------|--------|--------|--------|------------|--------|-------|
| $\xi_1$     | -1.19611 | -1.081107 | -1.16954 | -1.09537 | -0.90196 | -0.85518 |
| $\xi_2$     | 0.004153 | 0.003311 | 0.003612 | 0.003623 | 0.003595 | 0.0031199 |
| $\xi_3$     | 7.684E-5 | 4.239E-5 | 5.671E-5 | 5.927E-5 | 9.800E-5 | 7.2947E-5 |
| $\xi_4$     | -1.504E-4 | -1.469E-4 | -9.540E-5 | -1.192E-4 | -1.348E-4 | -1.560E-4 |
| $\lambda$   | 24 | 21.71831 | 13.92213 | 19.54295 | 14.0211 | 13.0486 |
| $R_e$ (Ω)   | 0.0008 | 0.000491 | 0.0008 | 0.000735 | 0.0005923 | 0.0004943 |
| $B(V)$      | 0.072756 | 0.08265 | 0.020932 | 0.024743 | 0.027341 | 0.028672 |
| $j_n$ (mA/cm²) | 30 | 29.99945 | 1.1147 | 4.07185 | 30 | 29.8682 |
| $j_{max}$ (mA/cm²) | 862.27594 | 1010.70957 | 872.68143 | 1170.406 | 952.8972 | 794.9896 |
| $\epsilon$ (μm) | 199.59871 | 162.26927 | 200 | 176.17291 | 187.8705 | 177.1509 |
| $A$ (cm²)   | 100 | 85.52841 | 85.66426 | 63.76876 | 85.0404 | 97.6386 |
| $F_{obj}$   | 4.2751e-5 | 9.2823E-5 | 8.4986E-5 | 8.4455E-5 | 3.0926E-5 | 2.5833E-5 |

6. CONCLUSION

In this paper, ALO and DA are proposed to extract the optimized parameters of PEMFC electrochemical model which is one of the most popular PEMFC model. The methodology is applied to Ballard Mark V PEMFC. Through the analysis results of both algorithms, reveals that ALO is better than DA. In addition, the accuracy of the optimized parameters is compared with the results reported in the Ref. [10]. Both algorithms produced much lower MSE and can be competent applicants to conquer the complexity of PEMFC parameter estimation problem. However, observing the convergence curve for the best results of each fuel cell reveals that both algorithms are easy to entrap at local optima for short period of time. This will cost the time to reach the global optimum and sometime lead to premature convergence. Nevertheless, ALO shows better efficiency on converging to the objective functions. However, for DA further modification on the parameter selection can be done to improve the converging issue. Furthermore, comparison in Table 2 reveals that ALO and DA have shown promising method on obtaining PEMFC model parameter. Some improvements can be introduced to existing framework of ALO and DA in order to overcomethe aforementioned drawbacks.

ACKNOWLEDGEMENTS

The author would like to credit University Malaysia Perlis for providing aid through project supervision and permission to use Center of Excellent for Renewable Energy (CERE), School of Electrical System Engineering facilities and equipment.

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