LEARNING TO SIMULATE

Nataniel Ruiz 1, Samuel Schulte 2, Mannohan Chandraker 2
1Department of Computer Science, Boston University
2NEC-Labs
nrui9@bu.edu, {samuel,manu}@nec-labs.com

ABSTRACT

Simulation is a useful tool in situations where training data for machine learning models is costly to annotate or even hard to acquire. In this work, we propose a reinforcement learning-based method for automatically adjusting the parameters of any (non-differentiable) simulator, thereby controlling the distribution of synthesized data in order to maximize the accuracy of a model trained on that data. In contrast to prior art that handcrafts these simulation parameters or adjusts only parts of the available parameters, our approach fully controls the simulator with the actual underlying goal of maximizing accuracy, rather than mimicking the real data distribution or randomly generating a large volume of data. We find that our approach (i) quickly converges to the optimal simulation parameters in controlled experiments and (ii) can indeed discover good sets of parameters for an image rendering simulator in actual computer vision applications.

1 INTRODUCTION

In order to train deep neural networks, significant effort has been directed towards collecting large-scale datasets for tasks such as machine translation (Luong et al., 2015), image recognition (Deng et al., 2009) or semantic segmentation (Geiger et al., 2013; Cordts et al., 2016). It is, thus, natural for recent works to explore simulation as a cheaper alternative to human annotation (Gaidon et al., 2016; Ros et al., 2016; Richter et al., 2016). Besides, simulation is sometimes the most viable way to acquire data for rare events such as traffic accidents. However, while simulation makes data collection and annotation easier, it is still an open question what distribution should be used to synthesize data. Consequently, prior approaches have used human knowledge to shape the generating distribution of the simulator (Sakaridis et al., 2018), or synthesized large-scale data with random parameters (Richter et al., 2016). In contrast, this paper proposes to automatically determine simulation parameters such that the performance of a model trained on synthesized data is maximized.

Traditional approaches seek simulation parameters that try to model a distribution that resembles real data as closely as possible, or generate enough volume to be sufficiently representative. By learning the best set of simulation parameters to train a model, we depart from the above in three crucial ways. First, the need for laborious human expertise to create a diverse training dataset is eliminated. Second, learning to simulate may allow generating a smaller training dataset that achieves similar or better performances than random or human-synthesized datasets (Richter et al., 2016), thereby saving training resources. Third, it allows questioning whether mimicking real data is indeed the best use of simulation, since a different distribution might be optimal for maximizing a test-time metric (for example, in the case of events with a heavy-tailed distribution).

More formally, a typical machine learning setup aims to learn a function $h_{\theta}$ that is parameterized by $\theta$ and maps from domain $\mathcal{X}$ to range $\mathcal{Y}$, given training samples $(x, y) \sim p(x, y)$. Data $x$ usually arises from a real world process (for instance, someone takes a picture with a camera) and labels $y$ are often annotated by humans (someone describing the content of that picture). The distribution $p(x, y)$ is assumed unknown and only an empirical sample $D = \{(x_i, y_i)\}_{i=1}^N$ is available.

The simulator attempts to model a distribution $q(x, y; \psi)$. In prior works, the aim is to adjust the form of $q$ and parameters $\psi$ to mimic $p$ as closely as possible. In this work, we attempt to automatically learn the parameters of the simulator $\psi$ such that the loss $\mathcal{L}$ of a machine learning model $h_{\theta}$ is minimized over some validation data set $D_{\text{val}}$. This objective can be formulated as the bi-level
optimization problem

\[
\psi^* = \arg \min_{\psi} \sum_{(x,y) \in D_{val}} \mathcal{L}(y, h_\theta(x; \theta^*(\psi)))
\]

(1a)

s.t. \( \theta^*(\psi) = \arg \min_{\theta} \sum_{(x,y) \in D_{val}} \mathcal{L}(y, h_\theta(x, \theta)) \),

(1b)

where \( h_\theta \) is parameterized by model parameters \( \theta \), \( D_{q(x,y|\psi)} \) describes a data set generated by the simulator and \( \theta(\psi) \) denotes the implicit dependence of the model parameters \( \theta \) on the model's training data and consequently, for synthetic data, the simulation parameters \( \psi \). In contrast to Fan et al. (2018), who propose a similar setup, we focus on the actual data generation process \( q(x,y; \psi) \) and are not limited to selecting subsets of existing data. In our formulation, the upper-level problem (equation 1a) can be seen as a meta-learner that learns how to generate data (by adjusting \( \psi \)) while the lower-level problem (equation 1b) is the main task model (MTM) that learns to solve the actual task at hand. In Section 2, we describe an approximate algorithm based on policy gradients (Williams 1992) to optimize the objective 1. Since we must work with a black-box simulator, an interface is required for the algorithm to interact with it, which is also described in Section 2.

In various experiments on both toy data and real computer vision problems, Section 4 analyzes different variants of our approach and investigates interesting questions, such as: “Can we train a model \( h_\theta \) with less but targeted high-quality data?” or “Are simulation parameters that approximate real data the optimal choice for training models?” The experiments indicate that our approach is able to quickly identify good scene parameters \( \psi \) that compete and in some cases even outperform the actual validation set parameters for synthetic as well as real data, on computer vision problems such as object counting or semantic segmentation.

2 Method

2.1 Problem Statement

Given a simulator that samples data as \((x, y) \sim q(x, y; \psi)\), our goal is to adjust \( \psi \) such that the MTM \( h_\theta \) trained on that simulated data minimizes the risk on real data \((x, y) \sim p(x, y)\). Assume we are given a validation set from real data \( D_{val} \) and we can sample synthetic datasets \( D_{q(x,y|\psi)} \sim q(x, y; \psi) \). Then, we can train \( h_\theta \) on \( D_{q(x,y|\psi)} \) by minimizing equation 1b

Note the explicit dependence of the trained model parameters \( \theta^* \) on the underlying data generating parameters \( \psi \) in equation 1b. To find \( \psi^* \), we minimize the empirical risk over the held-out validation set \( D_{val} \) as defined in equation 1a. Our desired overall objective function can thus be formulated as the bi-level optimization problem in equation 1.

Attempting to solve it with a gradient-based approach poses multiple constraints on the lower-level problem 1b like smoothness, twice differentiability and an invertible Hessian (Bracken & McGill 1973; Colson et al. 2007). For our case, even if we choose the model \( h_\theta \) to fulfill these constraints, the objective would still be non-differentiable as we (i) sample from a distribution that is parameterized by the optimization variable and (ii) the underlying data generation process (e.g., an image rendering engine) is assumed non-differentiable for the sake of generality of our approach. In order to cope with the above defined objective, we resort to a reinforcement learning approach and use policy gradients (Williams 1992) to optimize \( \psi \).

2.2 Learning to Simulate Data with Policy Gradients

Our goal is to generate a synthetic dataset such that the main task model (MTM) \( h_\theta \), when trained on this dataset until convergence, achieves maximum accuracy on the test set. The test set is evidently not available during train time. Thus, the task of our algorithm is to maximize MTM’s performance on the validation set by generating suitable data. Similar to reinforcement learning, we define a policy \( \pi_\omega \) parameterized by \( \omega \) that can sample parameters \( \psi \sim \pi_\omega \) for the simulator. The simulator can be seen as a generative model \( G(x, y; \psi) \) which generates a set of data samples \((x, y)\) conditioned on \( \psi \). We provide more details on the interface between the policy and the data generating function in the following section and give a concrete example for computer vision applications in Section 4.
policy receives a reward that we define based on the accuracy of the trained MTM on the validation set. Figure 1 provides a high-level overview.

Specifically, we want to maximize the objective

$$J(\omega) = \mathbb{E}_{\psi \sim \pi(\omega)} [R]$$

with respect to $\omega$. The reward $R$ is computed as the negative loss $L$ or some other accuracy metric on the validation set. Following the REINFORCE rule (Williams, 1992) we obtain gradients for updating $\omega$ as

$$\nabla_\omega J(\omega) = \mathbb{E}_{\psi \sim \pi(\omega)} \left[ \nabla_\omega \log(\pi(\psi)) R(\psi) \right].$$

An unbiased, empirical estimate of the above quantity is

$$\mathcal{L}(\omega) = \frac{1}{K} \sum_{k=1}^{K} \nabla_\omega \log(\pi(\psi)) \hat{A}_k,$$

where $\hat{A}_k = R(\psi_k) - b$ is the advantage estimate and $b$ is a baseline (Williams, 1992) that we choose to be an exponential moving average over previous rewards. In this empirical estimate, $K$ is the number of different datasets $D_{q(x,y|\psi)}$ sampled in one policy optimizing batch and $R(\psi_k)$ designates the reward obtained by the $k$-th MTM trained until convergence.

Given the basic update rule for the policy $\pi(\omega)$, we can design different variants of our algorithm for learning to simulate data by introducing three control knobs. First, we define the number of training epochs $\xi$ of the MTM in each policy iteration as a variable. The intuition is that a reasonable reward signal may be obtained even if MTM is not trained until full convergence, thus reducing computation time significantly. Second, we define the size $M$ of the data set generated in each policy iteration. Third, we either choose to retain the MTM parameters $\theta$ from the previous iteration and fine-tune on the newly created data or we estimate $\theta$ from scratch (with a random initialization). This obviously is a trade-off because by retaining parameters the model has seen more training data in total but, at the same time, may be influenced by suboptimal data in early iterations. We explore the impact of these three knobs in our experiments. Algorithm 1 summarizes our approach.

for iteration=1,2,... do
  Use policy $\pi(\omega)$ to generate $K$ model parameters $\psi_k$
  Generate $K$ datasets $D_{q(x,y|\psi_k)}$ of size $M$ each
  Train or fine-tune $K$ main task models (MTM) for $\xi$ epochs on data provided by $\mathcal{M}_k$
  Obtain rewards $R(\psi_k)$, i.e., the accuracy of the trained MTMs on the validation set
  Compute the advantage estimate $\hat{A}_k = R(\psi_k) - b$
  Update the policy parameters $\omega$ via equation 4
end

Algorithm 1: Our approach for “learning to simulate” based on policy gradients.

2.3 Interfacing a Simulator with the Policy

We defined a general black-box simulator as a distribution $G(x, y | \psi)$ over data samples $(x, y)$ parameterized by $\psi$. In practice, a simulator is typically composed of a deterministic “rendering”
process and a sampling step as \(G(x, y | \psi) = R(S(\rho | \psi), P(\phi))\), where the actual data description \(\rho\) (e.g., what objects are rendered in an image) is sampled from the provided simulation parameters \(\psi\) and specific rendering settings \(\phi\) (e.g., lighting conditions) are sampled from some prior. To enable efficient sampling (via ancestral sampling) (Bishop, 2006), the data description distribution is often modeled as a Bayesian network (directed acyclic graph) where \(\psi\) defines the parameters of the distributions in each node, but more complex models are possible too.

The interface to the simulator is thus \(\psi\) which describes parameters of the internal probability distributions of the black-box simulator. Note that \(\psi\) can be modeled as an unconstrained continuous vector and still describe various probability distributions. For instance, a continuous Gaussian is modeled by its mean and variance. A K-dimensional discrete distribution is modeled with K real values. We assume the black-box normalizes the values to a proper distribution via a softmax.

With this convention all input parameters to the simulator are unconstrained continuous variables. We thus model our policy as the multivariate Gaussian \(\pi_\omega(\rho) = N(\omega, \sigma^2)\) with as many dimensions as simulation parameters \(\rho\). For simplicity, we only optimize for the mean and set the variance to 0.05 in all cases, although the policy gradients defined above can handle both. Note that our policy can be extended to a more complicated form, e.g., by including the variance or by taking various contextual data as input and implementing the policy as a sequential model similar to (Zoph & Le, 2016).

3 DISCUSSION AND RELATED WORK

The proposed approach can be seen as a meta-learner that alters the data a machine learning model is trained on to achieve high accuracy on a validation set. This concept is similar to recent papers that learn policies for neural network architectures (Zoph & Le, 2016) and optimizers (Bello et al., 2017). In contrast to these works, we are focusing on the data generation parameters and actually create new, randomly sampled data in each iteration. While (Fan et al., 2018) proposes a subset selection approach for altering the training data, we are actually creating new data. This difference is important because we are not limited to a fixed probability distribution at data acquisition time. We can thus generate or oversample unusual situations that would otherwise not be part of the training data.

Similar to the above-mentioned papers, we also choose a variant of stochastic gradients (policy gradients (Williams, 1992)) to overcome the non-differentiable sampling and rendering and estimate the parameters of the policy \(\pi_\omega\). While alternatives for black-box optimization exist, like evolutionary algorithms (Salimans et al., 2017) or sampling-based methods (Bishop, 2006), we favor policy gradients in this work for their sample efficiency and success in prior art. Another direction to explore is to approximate the data-generation/rendering process in a differentiable way (Loper & Black, 2014), which may enable better training. However, for applications like computer vision, differentiable rendering (Loper & Black, 2014) cannot yet compete with more mature rendering engines in terms of data fidelity and expressive power.

When relying on simulated data for training machine learning models, the issue of “domain gap” between real and synthetic data arises. Many recent works (Ganin et al., 2016; Chen et al., 2017; Tsai et al., 2018) focus on bridging this domain gap, particularly for computer vision tasks. We believe the contributions of our work are orthogonal.

4 EXPERIMENTS

The intent of our experimental evaluation is (i) to illustrate the concept of our approach in a controlled toy experiment (section 4.1), (ii) to analyze different properties of the proposed algorithm 1 on a high-level computer vision task (section 4.3) and (iii) to demonstrate our ideas on real data for semantic image segmentation (section 4.5).

4.1 TOY EXPERIMENTS ON GAUSSIAN MIXTURES

To illustrate the concept of our proposed ideas we define a binary classification task on the 2-dimensional Euclidean space, where data distribution \(p(x, y | \psi_{\text{real}})\) of the two classes is represented by Gaussian mixture models (GMM) with 3 components, respectively. We generate validation and test sets from \(p(x, y | \psi_{\text{real}})\). Another GMM distribution \(q(x, y | \psi)\) reflects the simulator that generates
Figure 2: **Top row:** The decision boundaries (shaded areas) of a non-linear SVM trained on data generated by $q(x, y \mid \psi_i)$ for three different iterations $i$ of our policy $\pi_\omega$. The data points overlaid are the test set. **Bottom row:** Decision boundary when trained on data sampled from $p(x, y \mid \psi_{\text{real}})$ (left) and on the converged parameters $\psi^*$ (middle); Data sampled from $q(x, y \mid \psi^*)$ (right).

training data for the main task model (MTM) $h_\theta$, which is a non-linear SVM with RBF-kernels in this case. To demonstrate the practical scenario where a simulator is only an approximation to the real data, we fix the number of components per GMM in $\psi$ to be only 2 and let the policy $\pi_\omega$ only adjust mean and variances of the GMMs. Again, the policy adjusts $\psi$ such that the accuracy (i.e., reward $R$) of the SVM is maximized on the validation set.

The top row of figure 2 illustrates how the policy gradually adjusts the data generating distribution $q(x, y \mid \psi)$ such that reward $R$ is increased. The learned decision boundaries in the last iteration (right) well separate the test data. The bottom row of figure 2 shows the SVM decision boundary when trained with data sampled from $p(x, y \mid \psi_{\text{real}})$ (left) and with the converged parameters $\psi^*$ from the policy (middle). The third figure in the bottom row of figure 2 shows samples from $q(x, y \mid \psi^*)$.

To actually synthesize novel scenes, we first need a model $S(\rho \mid \psi)$ that allows to sample instances of scenes $\rho$ given parameters $\psi$ of the probability distributions of the scene model. Recall that $\psi$ is produced by our learned policy $\pi_\omega$.

Our traffic scene model $S(\rho \mid \psi)$ handles different types of intersections, various car models driving on the road, road layouts, buildings on the side or weather conditions. Please see the appendix for more details. In our experiments, the model is free to adjust some of the variables, e.g., the probability of cars being on the road, while we keep others at a fixed distribution, e.g., the weather conditions. These fixed distributions are considered the rendering parameters $\phi$ and modeled with a uniform distribution as $P(\phi)$. Given these two distributions, we can sample a new scene and render it as $R(S(\rho \mid \psi), P(\phi))$. Figure 3 shows examples of rendered scenes.
Figure 3: Example of rendered traffic scene with CARLA (Dosovitskiy et al., 2017) and the Unreal engine (Epic-Games, 2018).

Figure 4: (a) shows the reward on the validation set evolving over policy iterations. (b) shows the reward on the unseen test set. We observe that even when using the “adversarial” initialization of parameters, our approach converges to the same reward $R$, but at a slower rate. (c) shows the reward on the unseen test for different random parameter initializations.

4.3 LEARNING TO SIMULATE ON A HIGH-LEVEL VISION TASK

As a first high-level computer vision task we choose counting cars in rendered images, where the goal is to train a convolutional neural network $h_{\theta}$ to count all instances individually for different types of cars in an image. The evaluation metric and (also the loss) is the $\ell_1$ distance between predicted and ground truth count, averaged over the different car types. The reward $R$ is the negative $\ell_1$ loss. For this experiment, we generate validation and test sets with a fixed and pre-defined distribution $\psi_{\text{real}}$.

Initialization: We first evaluate our proposed policy (dubbed “lts” in the figures) for two different initializations, a standard random one and a deliberately adversarial one (compared to validation and test sets), and we also compared with a model trained on a data set sampled with $\psi_{\text{real}}$, i.e., the test set parameters. Figure 4 explains our results. We can see in figure 4a that our policy $\pi_{\omega}$ (“lts”) quickly reaches high reward $R$ on the validation set, equal to the reward we get when training models with $\psi_{\text{real}}$. Figure 4b shows that high rewards are also obtained on the test set for both initializations, albeit convergence is slower for the adversarial initialization. The reward after convergence is comparable to the model trained on $\psi_{\text{real}}$. Since our policy $\pi_{\omega}$ is inherently stochastic, we show in figure 4c convergence for different random initializations and observe a very stable behavior.

Accumulating data: Next, we explore the difference between training the MTM $h_{\theta}$ from scratch in each policy iteration or retaining its parameters and fine-tune, see algorithm 1. We call the second option the “accumulated main task model (AMTM)” because it is not re-initialized and accumulates information over policy iterations. The intention of this experiment is to analyze the situation where the simulator is used for generating large quantities of data, like in (Richter et al., 2016). First, by comparing figures 4b and 5a, we observe that the reward $R$ gets significantly higher than when training MTM from scratch in each policy iteration. Note that we still use the MTM reward as our training signal, we only observe the AMTM reward for evaluation purposes.

For the case of accumulating the MTM parameters, we further compare with two baselines. First, replicating a hand-crafted choice of simulation parameters, we assume no domain expertise and randomly sample simulator parameters (within a sensible range) in each iteration (“random policy params”). Second, we take the parameters given by our learned policy after convergence (“final policy params”) as a stronger baseline. For reference, we train another AMTM with the ground truth validation set parameters (“validation params”). All baselines are accumulated main task models, but with fixed parameters for sampling data, i.e., resembling the case of generating large datasets. We can see from figure 5a that our approach gets very close to the ground truth validation set parameters.
and significantly outperforms the random parameter baseline. Interestingly, “lts” even outperforms the “final policy params” baseline, which we attribute to increased variety of the data distribution. Again, “lts” converges to a high reward $R$ even with an adversarial initialization, see figure 5b.

**Dataset size:** Next, we explore the parameter $M$ of our algorithm that controls the dataset size generated in each policy iteration. For example, when $M = 100$, we generate at each policy step a dataset of 100 images using the parameters from the policy which are then used to train our main task model $h_\theta$. We evaluate policies with sizes 20, 50, 100 and 200. For a fair comparison, we generate 40,000 images with our final learned set of parameters and train $h_\theta$ for 5 epochs and evaluate on the test set. We observed that for this task a dataset size of just 20 suffices for our model to converge to good scene parameters $\psi$, which is highly beneficial for the wall-time convergence speed. Having less data per policy iteration means faster training of the MTM $h_\theta$.

**Number of epochs:** Similar to the previous experiment, we now analyze the impact of the number of epochs $\xi$ used to train the main task model $h_\theta$. The setup is similar to the previous experiment: We generate 40,000 images with our final learned set of parameters and train $h_\theta$ for a fixed number of epochs and evaluate on the test set. Figure 5c shows the reward of the accumulated MTM for four different values of $\xi$ (1, 3, 7, 10). Our conclusion, for the car-counting task, is that learning to simulate is robust to lower training epochs, which means that even if the MTM has not fully converged yet the reward signal is good enough to provide guidance for our system, again leading to a potential wall-time speed up of the overall algorithm. All four cases converge, including the one where we train the MTM for only one epoch. Note that this is dependent on the task at hand, and a more complicated task might necessitate convergence of the main task model to provide discriminative rewards.

### 4.4 Semantic Segmentation on Simulated Data

For the next set of experiments we use semantic segmentation as our test bed, which aims at predicting a semantic category for each pixel in a given RGB image (Chen et al., 2018). Our modified CARLA simulator (Dosovitskiy et al., 2017) provides ground truth semantic segmentation maps for generated traffic scenes, including categories like road, sidewalk or cars. For the sake of these experiments, we focus on the segmentation accuracy of cars, measured as intersection-over-union (IoU), and allow our policy $\pi_\omega$ to adjust parameters related to cars to maximize reward $R$ (i.e., car IoU). This includes the probability of generating different types of cars, but also the length of the road because the more road available, the more cars can be placed in the scene. The main task model $h_\theta$ is a CNN that takes a rendered RGB image as input and predicts a per-pixel classification output.

We first generate validation set parameters $\psi_{\text{val}}$ that reflect traffic scenes moderately crowded with cars, random intersections and buildings on the side. As a reference point for our proposed algorithm, we sample a few data sets with the validation set parameters $\psi_{\text{val}}$, train MTMs and report the maximum reward (IoU of cars) achieved. We compare this with our learned policy $\pi_\omega$, and can observe in figure 6a that it actually outperforms the validation set parameters. This is an interesting observation because it shows that the validation set parameters $\psi_{\text{val}}$ may not always be the optimal
Figure 6: (a) Reward curves of our approach compared to a model trained on data generated with the actual validation set parameters on the synthetic semantic segmentation task. (b) Reward curves on the real validation set of KITTI for semantic segmentation. We plot the learning-to-simulate, and the mean and maximum car IoUs obtained using scenes generated with 10 sets of random parameters.

| Generative Parameters | Car IoU       |
|-----------------------|--------------|
| random params         | 0.260 ± 0.037|
| learned params        | 0.334 ± 0.019|

Table 1: Mean value of Car IoU on the KITTI test set for models $h_\theta$ trained from synthetic data generated by random or learned parameters.

4.5 Semantic Segmentation on Real Data

We finally demonstrate the practical impact of our learning-to-simulate approach on semantic segmentation on KITTI (Geiger et al., 2013) by training a main task model (MTM) $h_\theta$ with a reward signal coming from real data. Using simulated data for semantic segmentation was recently investigated from a domain adaptation perspective (Tsai et al., 2018; Richter et al., 2016), where an abundant set of simulated data is leveraged to train models applicable on real data. Here, we investigate targeted generation of simulated data and its impact on real data. Since the semantic label space of KITTI and our CARLA simulator are not identical, we again focus on segmentation of cars by measuring IoU for that category. The form of the main task model $h_\theta$ is the same as in the previous experiment.

Note that for real data, we actually do not have access to the underlying data generating parameters $\psi_{\text{real}}$. Our baselines in this experiments use training data generated by the simulator with random parameters sampled within a range to generate sensible scenes with a moderate amount of cars. However, it is important to mention that is unclear and hard to guess what parameters are actually good for training an MTM $\theta$, making our automatic approach attractive in such situations. Figure 6b shows the rewards obtained by all methods on the validation set, where we observe that learning-to-simulate outperforms mean and max of the baseline models trained on samples from the random parameters. The results on the real KITTI test set in table 1 confirm the superior results of learning-to-simulate. We use a set of 10 sampled datasets for random and learned parameters and display the mean value of the Car IoU metric across these sampled datasets.

5 Conclusion

Learning to simulate can be seen as a meta-learning algorithm that adjusts parameters of a simulator to generate synthetic data such that a machine learning model trained on this data achieves high accuracies on validation and test sets, respectively. Given the need for large-scale data sets to feed deep learning models and the often high cost of annotation and acquisition, we believe our approach is a sensible avenue for practical applications to leverage synthetic data. Our experiments illustrate the concept and demonstrate the capability of learning to simulate on both synthetic and real data.
REFERENCES

Irwan Bello, Barret Zoph, Vijay Vasudevan, and Quoc V Le. Neural optimizer search with reinforcement learning. In *International Conference on Machine Learning*, pp. 459–468, 2017.

Christopher M. Bishop. *Pattern Recognition and Machine Learning (Information Science and Statistics)*. Springer-Verlag, Berlin, Heidelberg, 2006. ISBN 0387310738.

Jerome Bracken and James T. McGill. Mathematical Programs with Optimization Problems in the Constraints. *Operations Research*, 21:37–44, 1973.

Liang-Chieh Chen, Yukun Zhu, George Papandreou, Florian Schroff, and Hartwig Adam. Encoder-decoder with atrous separable convolution for semantic image segmentation. In *ECCV*, 2018.

Yi-Hsin Chen, Wei-Yu Chen, Yu-Ting Chen, Bo-Cheng Tsai, Yu-Chiang Frank Wang, and Min Sun. No more discrimination: Cross city adaptation of road scene segmenters. In *The IEEE International Conference on Computer Vision (ICCV)*, Oct 2017.

Benoît Colson, Patrice Marcotte, and Gilles Savard. An overview of bilevel optimization. *Annals of Operations Research*, 153(1):235–256, 2007.

Marius Cordts, Mohamed Omran, Sebastian Ramos, Timo Rehfeld, Markus Enzweiler, Rodrigo Benenson, Uwe Franke, Stefan Roth, and Bernt Schiele. The cityscapes dataset for semantic urban scene understanding. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pp. 3213–3223, 2016.

Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. Imagenet: A large-scale hierarchical image database. In *Computer Vision and Pattern Recognition, 2009. CVPR 2009. IEEE Conference on*, pp. 248–255. Ieee, 2009.

Alexey Dosovitskiy, German Ros, Felipe Codevilla, Antonio López, and Vladlen Koltun. Carla: An open urban driving simulator. *arXiv preprint arXiv:1711.03938*, 2017.

Epic-Games. Epic Games unreal engine 4. [https://www.unrealengine.com](https://www.unrealengine.com), 2018. Accessed: 2018-09-27.

Yang Fan, Fei Tian, Tao Qin, Xiang-Yang Li, and Tie-Yan Liu. Learning to teach. In *International Conference on Learning Representations*, 2018. URL [https://openreview.net/forum?id=HJewuJWCZ](https://openreview.net/forum?id=HJewuJWCZ).

Adrien Gaidon, Qiao Wang, Yohann Cabon, and Eleonora Vig. Virtual worlds as proxy for multi-object tracking analysis. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pp. 4340–4349, 2016.

Yaroslav Ganin, Evgeniya Ustinova, Hana Ajakan, Pascal Germain, Hugo Larochelle, François Laviolette, Mario Marchand, and Victor Lempitsky. Domain-adversarial training of neural networks. *J. Mach. Learn. Res.*, 17(1):2096–2030, January 2016. ISSN 1532-4435. URL [http://dl.acm.org/citation.cfm?id=2946645.2946704](http://dl.acm.org/citation.cfm?id=2946645.2946704).

Andreas Geiger, Philip Lenz, Christoph Stiller, and Raquel Urtasun. Vision meets robotics: The kitti dataset. *The International Journal of Robotics Research*, 32(11):1231–1237, 2013.

Matthew M Loper and Michael J Black. Opendr: An approximate differentiable renderer. In *European Conference on Computer Vision*, pp. 154–169. Springer, 2014.

Minh-Thang Luong, Hieu Pham, and Christopher D. Manning. Effective approaches to attention-based neural machine translation. In *Empirical Methods in Natural Language Processing (EMNLP)*, pp. 1412–1421, Lisbon, Portugal, September 2015. Association for Computational Linguistics. URL [http://aclweb.org/anthology/D15-1166](http://aclweb.org/anthology/D15-1166).

Matthias Mueller, Vincent Casser, Jean Lahoud, Neil Smith, and Bernard Ghanem. Ue4sim: A photo-realistic simulator for computer vision applications. *arXiv preprint arXiv:1708.05869*, 2017.

Stephan R Richter, Vibhav Vineet, Stefan Roth, and Vladlen Koltun. Playing for data: Ground truth from computer games. In *European Conference on Computer Vision*, pp. 102–118. Springer, 2016.
German Ros, Laura Sellart, Joanna Materzynska, David Vazquez, and Antonio M Lopez. The synthia dataset: A large collection of synthetic images for semantic segmentation of urban scenes. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pp. 3234–3243, 2016.

Samuel Rota Bulo, Gerhard Neuhold, and Peter Kontschieder. Loss max-pooling for semantic image segmentation. In *The IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, July 2017.

Christos Sakaridis, Dengxin Dai, and Luc Van Gool. Semantic foggy scene understanding with synthetic data. *International Journal of Computer Vision*, 126(9):973–992, 2018. doi: 10.1007/s11263-018-1072-8.

Tim Salimans, Jonathan Ho, Xi Chen, Szymon Sidor, and Ilya Sutskever. Evolution strategies as a scalable alternative to reinforcement learning. *arXiv preprint arXiv:1703.03864*, 2017.

Shital Shah, Debadeepta Dey, Chris Lovett, and Ashish Kapoor. Airsim: High-fidelity visual and physical simulation for autonomous vehicles. In *Field and service robotics*, pp. 621–635. Springer, 2018.

Yi-Hsuan Tsai, Wei-Chih Hung, Samuel Schulter, Kihyuk Sohn, Ming-Hsuan Yang, and Manmohan Chandraker. Learning to adapt structured output space for semantic segmentation. In *The IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, June 2018.

Ronald J Williams. Simple statistical gradient-following algorithms for connectionist reinforcement learning. *Machine learning*, 8(3-4):229–256, 1992.

Barret Zoph and Quoc V Le. Neural architecture search with reinforcement learning. *arXiv preprint arXiv:1611.01578*, 2016.
Figure 7: Test and validation error from main task networks trained on 40,000 images during 5 epochs using final learned parameters for different sizes of datasets generated per policy iteration.

A TRAFFIC SCENE MODEL

Our model comprises the following elements:

- A straight road of variable length.
- Either an L, T or X intersection at the end of the road.
- Cars of 5 different types which are spawned randomly on the straight road.
- Houses of a unique type which are spawned randomly on the sides of the road.
- Four different types of weather.

All of these elements are tied to parameters: $\rho_k$ can be decomposed into parameters which regulate each of these objects. The scene is generated "block" by "block". A block consists of a unitary length of road with sidewalks. Buildings can be generated on both sides of the road and cars can be generated on the road. $\rho_{k,\text{car}}$ designates the probability of car presence in any road block. Cars are sampled block by block from a Bernoulli distribution $X \sim \text{Bern}(\rho_{k,\text{car}})$. To determine which type of car is spawned (from our selection of 5 cars) we sample from a Categorical distribution determined by 5 parameters $\rho_{k,\text{car}}$ where $i$ is an integer representing the identity of the car and $i \in [1, 5]$. $\rho_{k,\text{house}}$ designates the probability of house presence in any road block. Houses are sampled block by block from a Bernoulli distribution $X \sim \text{Bern}(\rho_{k,\text{house}})$.

Length to intersection is sampled from a Categorical distribution determined by 10 parameters $\rho_{k,\text{length}}$, with $i \in [8, 18]$ where $i$ denotes the length from the camera to the intersection in "block" units. Weather is sampled randomly from a Categorical distribution determined by 4 parameters $\phi_{k,\text{weather}}$, where $i$ is an integer representing the identity of the weather and $i \in [1, 4]$. L, T and X intersections are sampled randomly with equal probability.

B CAR COUNTING DATASET SIZE

We explore the parameter $M$ of our algorithm that controls the dataset size generated in each policy iteration. In figure 7 we show a comparative graph of final errors on the validation and test sets for different values of $M$. For a fair comparison, we generate 40,000 images with our final learned set of parameters and train $h_\theta$ for 5 epochs. All values of $M$ used resulted in very similar errors in the validation and test set, we conclude that learning to simulate is robust to the $M$ when used on the car counting task.

C REPRODUCIBILITY

Since our method is stochastic in nature we verify that "learning to simulate" converges in the car counting task using different random seeds. We observe in figure 8a that the reward converges to the same value with three different random seeds. Additionally, in figure 8b, we observe that the accumulated main task network test reward also converges with different random seeds.
Figure 8: Main task network reward and accumulated MTN reward converge using different random seeds.