Large ion Coulomb crystals: A near-ideal medium for coupling optical cavity modes to matter

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We present an investigation of the coherent coupling of various transverse field modes of an optical cavity to ion Coulomb crystals. The obtained experimental results, which include the demonstration of identical collective coupling rates for different transverse modes of a cavity field to ions in the same large Coulomb crystal, are in excellent agreement with theoretical predictions. The results furthermore suggest that Coulomb crystals in the future may serve as near-ideal media for high-fidelity multimode quantum information processing and communication purposes, including the generation and storage of single-photon qubits encoded in different transverse modes.

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For the field of quantum information to mature to a practical stage, where complex computational tasks [1] and quantum information networks [2] can be realized, careful attention has to be paid to the actual quality of the physical systems involved. While the ideal system for carrying out serious quantum computational tasks has yet to be singled out, photons remain uncontested in their position as the ideal carriers of quantum information over large distances. Consequently, there is a clear need for identifying high quality physical media suitable for, e.g., single-photon generation and storage as well as for the realization of quantum repeaters.

While various systems continue to be investigated (see Ref. [2] and references therein), a single ion in an optical cavity appears to be an excellent candidate for such realizations [3–6]. In addition, larger ensembles of cold trapped ions in the form of so-called Coulomb crystals [7–9] in cavities may afford new opportunities for not only single-mode but also multimode quantum information purposes due to the combination of their solid-state properties, including long-term stability and uniform ion density throughout the crystal and their single isolated particle features, i.e., no significant internal state perturbations due to interactions between the individual ions [10]. These features are relevant for, e.g., encoding quantum information in orthogonal transverse spatial modes in contrast to the usual application of frequency and polarization degrees of freedom [11,12]. In addition, coupling to multiple modes may have applications even outside of the context of quantum information, for, e.g., quantum imaging [13,14] and cavity mediated cooling [15–17].

Important steps toward the realization of high quality single-mode quantum devices based on an ion Coulomb crystal in a cavity were very recently taken by demonstrating that the collective strong coupling regime of cavity quantum electrodynamics [18] can be reached with large ion Coulomb crystals interacting with a cavity field at the single-photon level in the fundamental TEM_{00} mode of an optical cavity [10].

In this Rapid Communication, the potential of ion Coulomb crystals as a media for multimode quantum interfaces is explored by a thorough experimental investigation characterizing the coupling of the TEM_{00} and TEM_{10,01} transverse cavity-mode fields at the single-photon level to ion Coulomb crystals of various dimensions.

Using needle shaped crystals aligned along the cavity axis with a diameter smaller than the waist characterizing the Hermite-Gaussian TEM_{mn} field modes, detailed information on the coupling strength can be obtained through changing the position of the Coulomb crystal in the plane perpendicular to the cavity axis. Since through this procedure the crystal is moved into regions of dramatically varying micromotion induced by the trapping fields, the influence of this quiver motion on the coupling strength can be judged. In complementary experiments, the scaling of the coupling strength with respect to the crystals radial size for different modes has been investigated using Coulomb crystals with the central axis kept fixed in position and length in order to determine if and when convergence of the coupling strengths is reached. Finally, a precise measure of the coherent coupling rate for both modes is obtained in the regime where the coupling is expected to be independent of the cavity field mode (i.e., the radius of the crystal is large compared to the cavity mode waist), and additionally the number of ions is sufficient to attain useful optical densities. Throughout, comparison with theory is made to find near-perfect agreement in all instances.

In Fig. 1(a) schematic of the experimental setup is shown. The trap used is a linear rf trap with an optical cavity incorporated in between the four segmented electrode rods [19], such that the cavity axis is parallel to the trap’s rf field-free axis (z axis). 40Ca+ ions are loaded into the trap via resonant two-photon photoionization [19] and subsequently Doppler cooled on the 4s^2S_{1/2}−2P_{1/2} transition using two counter-propagating 397 nm laser beams while repumped on the 3d^2D_{3/2}−4p^2P_{1/2} transition with a 866 nm laser beam [10]. After the ions are cooled into a crystalline state, they are prepared by optical pumping with an efficiency of ~97% into the m_{J}=+3/2 magnetic substate of the long-lived metastable D_{3/2} level [10]. The optical cavity consists of two mirrors with a radius of curvature of 10 mm, which are separated by 11.8 mm. The cavity has a finesse of 3000 for light at the wavelength of 866 nm used to induce the coupling to the 40Ca+ ions via the 3d^2D_{3/2}−4p^2P_{1/2} transition. The Hermite-Gaussian TEM_{mn} modes at this wavelength have a
natural linewidth, $\gamma=(2\pi)1.12$ MHz is the optical dipole decay rate of the 3d$^2D_{3/2}$-$4p^2P_{1/2}$ transition, and $\Delta$ is the detuning of the probe pulse with respect to the atomic resonance. For ion Coulomb crystals in a linear rf quadrupole trap, which typically have a spheroidal shape with an uniform density $\rho$ [9], the coherent coupling rate is given by

$$G_{mn}^2(x_0,y_0) = g^2 \rho \int d^2r \psi_{mn}^2(x-x_0,z)\psi_{mn}^2(y-y_0,z) \times \sin^2 \left[ k z - (m + n + 1) \tan^{-1} \frac{z}{z_R} \right] + k (x-x_0)^2 + (y-y_0)^2 \right] 2r(z),$$

where $x_0$ and $y_0$ represent the radial offsets of the crystal center with respect to the cavity mode symmetry axis, $g$ is the single-ion coupling strength at an antinode in the center of the fundamental TEM$_{00}$ mode, $V=4\pi R^2 L/3$ is the volume of the spheroid crystal with half-length $L$ and radius $R$, and $\psi_{mn}$ is the Hermite-Gaussian mode function.

$$\psi_{mn}(u,z) = \sqrt{\frac{w_0}{w(z)}} H_m \left( \frac{u}{{w(z)}} \right) \exp \left( -\frac{u^2}{w(z)^2} \right) \quad (u = x, y),$$

with $H_m$ being the $m$th Hermite polynomial, $w(z) = w_0(1+z^2/z_R^2)^{1/2}$, and $r(z) = z + z_R^2/z$.

Of particular relevance for evaluating the applicability of the system as a transverse multimode light-material interface is the case of $R \gg w_0$, in which according to Eq. (2) the coupling strengths of the different transverse modes to the crystal are expected to converge. However in order to achieve convergence, the effect of micromotion of the individual ions, including those located far from the trap axis, on the coupling strength must be negligible. To evaluate this effect, a thin needle-shaped spheroidal Coulomb crystal, with half length $L=240 \pm 1$ $\mu$m and radius $R=21 \pm 1$ $\mu$m [Fig. 2(a)], is translated radially across the cavity mode volume by the application of appropriate dc voltages to two of the segmented electrode rods [Fig. 1(b)]. The displacement of the crystal in the transverse (xy) plane is determined by imaging the 397 nm fluorescence light emitted during cooling onto two charge coupled device (CCD) cameras. [See sketch in Fig. 1(b).] The precision in reading the position of the crystal is $\pm 0.8$ $\mu$m [20].

In Fig. 2(b) the measured coupling strengths using the Coulomb crystal shown in Fig. 2(a) is presented in terms of $G_{mn}^2$ normalized to $G_{00}^2(x_0=0, y_0=0)$ for the TEM$_{00}$ and TEM$_{10}$ modes. For each position of the crystal, the coherent coupling strength is measured through the broadening of the probe pulse transmission signal [Eq. (1)] with the probe tuned to the atomic resonance ($\Delta=0$). The experimental data are shown to agree very well with the theoretical predictions of Eq. (2) with mode functions derived from the cavity geometry, the crystal size and shape obtained from CCD images and the density of the ions determined from the trapping parameters [20]. Since the amplitude of the radial micromotion increases with the ions’ distance from the rf-free z axis, strong systematic deviations would have been expected at
large displacements if micromotion was an issue. This result importantly indicates that the inevitable radial micromotion of ions in linear rf traps does not couple significantly into their axial motion.

To what extent ion Coulomb crystals constitute a near-ideal media with respect to coherent coupling to various cavity modes has further been investigated by measuring the coherent coupling strength using ion Coulomb crystals with a fixed length $2L=480$ µm but with varying radii. The resulting coherent coupling strengths for the TEM$_{00}$ and TEM$_{10}$ mode cases are shown in Fig. 3. The density of all the crystals is $\rho=3.8 \times 10^8$ cm$^{-3}$, and their rotational symmetry axes coincide with that of the cavity mode $[x_0=y_0=0$ in Eq. (2)]. As expected, the increase in the coupling strength as a function of the radius is slower for the TEM$_{10}$ than for the TEM$_{00}$ since ions at the center of the cavity mode contribute much less to the coupling for the former. However, the coupling strengths converge to the same value for both modes for crystals with large radii, in good agreement with the theoretical predictions of Eq. (2).

Finally, to carefully check the prospect of using large ion Coulomb crystals as a media for multimode light-matter interfacing, a precise measurement of the coherent coupling rates for both modes was obtained by again measuring the broadening of the probe pulse transmission signal but this time for a series of detunings of the probe pulse from atomic resonance, $\Delta$. To obtain high optical densities, in this experiment, a crystal with a larger density ($\rho=5.4 \times 10^8$ cm$^{-3}$) and almost twice the length ($2L=1.2$ mm) of the crystals used in the previous experiment was used. In Fig. 4, a projection image of this crystal is shown together with images indicating the position of the TEM$_{00}$ and TEM$_{10}$ modes applied in the experiments. The results are presented in Fig. 5 together with Lorentzian fits to the data based on Eq. (1). With
and $\gamma$ as free fitting parameters, we obtain $G_{00} = (2\pi)11.6 \pm 0.1$ MHz, $\gamma = (2\pi)11.3 \pm 0.3$ MHz and $G_{10} = (2\pi)11.5 \pm 0.1$ MHz, $\gamma = (2\pi)11.4 \pm 0.3$ MHz for the TEM$_{00}$ and TEM$_{10}$ mode, respectively. The collective coupling rates, $G_{00}$ and $G_{10}$, are strikingly identical. The obtained $G_{00}$ and $G_{10}$ correspond to optical depths $\Gamma^2/\kappa\gamma = 4.5$ but could easily be made larger as is presented in Ref. [10]. Furthermore, an equal coupling strength was also observed for the TEM$_{10}$ and TEM$_{01}$ mode, indicating that ion Coulomb crystals open up for, e.g., the possibility of storing photonic qubits encoded in a spatial basis spanned by these two modes.

In conclusion we have shown that ion Coulomb crystals are an ideal system for obtaining high and uniform coupling strengths to the field of an optical cavity independent of the transverse mode. The achieved excellent agreement between experimental data and theoretical predictions confirm that the presence of the rf-trapping fields does not significantly alter the coupling strengths even for ions far from the trap axis. These results combined with previously measured long collective Zeeman substate coherence times [10] clearly indicate that ion Coulomb crystals should be able to serve as near-ideal media for high-fidelity multimode quantum information processing and communication devices.

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