Modeling Star counts in the Monoceros stream 
and the Galactic anti-centre.

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ABSTRACT

Context. There is a continued debate as to the form of the outer disc of the Milky Way galaxy, which has important implications for its formation. Stars are known to exist at a galacto-centric distance of at least 20 kpc. However, there is much debate as to whether these stars can be explained as being part of the disc or whether another extra galactic structure, the so called Monoceros ring/stream, is required.

Aims. To examine the outer disc of the Galaxy toward the anti-centre to determine whether the star counts can be explained by the thin and thick discs alone.

Methods. Using Sloan star counts and extracting the late F and early G dwarfs it is possible to directly determine the density of stars out to a galacto-centric distance of about 25 kpc. These are then compared with a simple flared disc model.

Results. A flared disc model is shown to reproduce the counts along the line of sights examined, if the thick disc does not have a sharp cut off. The flare starts at a Galacto-centric radius of 16 kpc and has a scale length of 4.5 ± 1.5 kpc.

Conclusions. Whilst the interpretation of the counts in terms of a ring/stream cannot be definitely discounted, it does not appear to be necessary, at least along the lines of sight examined towards the anti centre.

Key words. Galaxy – disc, structure, stellar content

1. Introduction

The position of the Sun within the Galactic plane has made understanding the true form of the Galaxy difficult. In the last ten years the situation has improved, however, with the advent of deep large areas surveys. Surveys in the near IR such as 2MASS, UKIDSS or in the visible such as the Sloan Digital Sky Survey (SDSS, Newberg et al. 2002) have allowed a more precise modeling of the large scale structures of our Galaxy.

It is generally accepted that there is both a thin and thick stellar disc. The stellar density of the thin disc is exponential in height above the Galactic plane and radial distance. In the vicinity of the Sun it has a scale length of about 2.4 kpc, however the scale height depends on the source type. The
older sources have a scale height of around 185 pc, but for the younger sources it is considerably less than this. The density of the thick disc (Gilmore & Reid 1983) is also exponential but with a larger scale length and scale height (Bilir et al. 2008), although it has less than a tenth of the density of the thin disc on the plane in the vicinity of the Sun.

Of particular importance to our understanding of the Galaxy and its formation, is to determine what happens towards the outer edge of the disc. Robin et al. (1992), using visible images from the CFHT, suggested that Galaxy has a cut at galacto-centric radius ($R$) of 13.5 kpc when looking at $l = 179^\circ, b = -2.5^\circ$, as the stellar density drops rapidly beyond that point. López-Corredoira et al. (2002) using 2MASS data suggested that the drop in stellar density near the plane was not caused by a cut off, rather a flare in the disc and concluded that the disc did not have a well defined cut off to at least 15 kpc.

The most recent deep surveys such as the SDSS clearly show that there are stars out to at least $R=20$ kpc. Their distribution, however, is not consistent with a simple exponential disc particularly when looking 15 to 30 degrees from the plane. Some authors (Momany et al. 2006) suggest these can be explained by a flare of the disc. Many other authors, however, have preferred to attribute these sources to rings or streams beyond the edge of the disc. In particular, the sources being studied here have been attributed to the so called Monoceros ring/stream (Newberg et al. 2002; Rocha-Pinto et al. 2003; Conn et al. 2005, 2007, 2008). This has been associated to the remnants of a dwarf galaxy which was cannibalized by the Milky Way, and whose progenitor was associated to the Canis Major over-density (Martin et al. 2004; Martínez-Delgado et al. 2005; Bellazzini et al. 2006; Butler et al. 2007; de Jong et al. 2007; Conn et al. 2007). This ring runs approximately parallel to the galactic plane, in the latitude range $10 < |b| < 35 \text{ deg.}$, and over most of the second and third quadrants.

That stellar streams exist is well known, and that produced by the Sagittarius dwarf galaxy (Ibata et al. 1994) is probably the most well studied stream associated with the Milky Way. Its form and high angle to the Galactic Plane makes confusion with a Galactic component highly unlikely. However, the proposed Monoceros stream is a very different feature to the Sagittarius stream running, as it does, parallel to the Galactic plane. Furthermore, whilst the Sagittarius stream is clearly a dwarf galaxy, the progenitor of Monoceros in the over-density in Canis Major has also been questioned, as other authors have explained the excess star as an effect of the warped+flared disc of the Milky Way (Momany et al. 2004, 2006; López-Corredoira 2006; López-Corredoira et al. 2007).

In this paper we examine if, using a simple flared disc model as suggested by Momany et al. (2006), we can reproduce the form of the deep star counts seen 15 to 30 degrees off the plane in Galactic anti-centre region, without requiring the presence of extra-galactic streams.

2. The Method

For this work we wish to count sources at a $R < 25$ kpc towards the Galactic anti-centre and between 11 and 31 degrees off the plane.

By far the simplest method of determining the stellar density along a line of sight in the disc is by isolating a group of stars with the same colour and absolute magnitude within a colour mag-
nitude diagram. This allows the luminosity function to be replaced by a constant in the stellar statistics equation:

\[
A(m) \equiv \frac{dN(m)}{dm} = \frac{\ln 10}{5} \omega \rho[r(m)]r(m)^3, \tag{1}
\]

\[r(m) = 10^{(m-M+5)/5},\]

where \(\omega\) is the area of the solid angle in radians and \(r\) is the distance in parsecs; the differential star counts for each line of sight, \(A(m)\), can be immediately converted into density \(\rho(r)\).

In the near IR, the red clump giants have been successfully used as standard candles, particularly when looking in the inner Galaxy (López-Corredoira et al. 2002). However, the red clump stars in the outer disc at the distance of interest would appear at \(m_k = 15\) and so the local dwarfs with the same colour would completely dominate the counts at this magnitude (López-Corredoira et al. 2002).

As the areas of interest all lie well off the plane, then the extinction will be low (typically under 1 magnitude). Therefore, it is possible to use visible counts. An examination of the HR diagram shows that when the extinction is low, the late F and early G dwarfs can be isolated using colour with only minimal contamination from other sources with the same colour but different absolute magnitudes (sub dwarfs, galacto-centric radius giants etc). For this work we have selected the source between \(F8V\) and \(G5V\). This gives a range of \(g-r\) of 0.36 to 0.49 and a range of absolute magnitudes \(M_g = 4.2\) to 5.4 which makes the sources approximately \(m_g \sim 20\) at the distance of interest. By having a range of absolute magnitudes, then when the counts are converted to density vs distance there is some smoothing and this is not included in a model which assumes a single absolute magnitude. Although the selection used here is not as well defined as the red clump stars in the near IR, it still has a sufficiently small range in absolute magnitude that the smoothing has little effect and the above approximation remains valid. There will, however, be sufficient stars detected in the outer Galaxy to give meaningful statistics which would not be the case if a smaller range in absolute magnitudes were used. Earlier sources have not been included as these sources would belong to a younger population with a far smaller scale height, also the absolute magnitude changes far more rapidly with colour. Later sources would have significant giant contamination and again the absolute magnitude changes more rapidly with colour.

The areas selected for this work lie between 10 and 30 degrees from the plane and are within 40 degrees of the anti-centre. We have not extended the range of longitudes because of the Galactic warp. The warp means that, in effect the position of the Galactic plane varies with position in the Galaxy, and along the line of sight. Although the effect of warp is strongest towards the outer edge of the disc, where the plane can be over a kpc away from the expected position with no warp, it can be clearly seen in the counts within a few kpc of the Sun (Hammersley et al 1995, López-Corredoira et al. 2002, Momany et al. 2006). The models of the warp are normally simple, based on tilted rings, and in general these do provide a good representation of the star counts. However, in the very outer disc the models are harder to test, and a small error in the model can lead to a significant error to the predicted position of the plane, and hence the predicted densities. Therefore, we have limited the regions used for this work to those where the effect of the warp should be small and so can be ignored. It should be noted, however, that whilst it will be possible to ascertain whether a flare can reproduce the star counts seen in the outer disc, it will not be possible to accurately determine all
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Table 1. Lines of sight used.

| $l$ ($^\circ$) | $b$ ($^\circ$) | Area (deg$^2$) | Extinction $E(B-V)$ |
|---------------|---------------|----------------|--------------------|
| 150           | 15            | 1.94           | 0.25               |
| 180           | 11            | 0.45           | 0.241              |
| 183           | 21            | 1.22           | 0.054              |
| 183           | 31            | 3.27           | 0.052              |
| 223           | 20            | 1.00           | 0.035              |

Fig. 1. The CMD for the region $l = 183^\circ$, $b = 21^\circ$

of the parameters. When large scale deep star counts in the outer disc become available it will be possible to model the warp more accurately. Until then, however, great care must be taken when comparing models with counts in the outer disc.

A second reason for limiting the longitude is that the distance to the feature increases rapidly with distance from the anti-centre, making the sources fainter and appear closer to the plane so that there is less contrast with the other disc sources.

3. The Data

The source densities in these regions will be very low requiring square degrees of sky to be covered to provide sufficient counts to give reasonable statistics. Therefore, the data has been taken from the SDSS release DR7 (Abazajian et al. 2009) with regions ~ 1 square degree. As the regions are all well off the plane it has been assumed that the extinction is local and so all of the magnitudes have been corrected for extinction using the Galactic extinction model of Shlegel et al (1998). Furthermore, the extinction is relatively small and a small residual error will not significantly affect the results, although it would make the sources appear at the wrong distance. Table 1 shows the position and assumed extinctions. The positions $l = 183^\circ$, $b = 21^\circ$ and $l = 220^\circ$ where used by Newberg et al. (2002); and the position at $l = 150^\circ$ was used by Conn et al. (2005), to support their “Monoceros stream” hypothesis.
4. Results

Figure 1 shows the $g$ vs. $g - r$ colour magnitude diagram for the region $l = 183^\circ$, $b = 21^\circ$ with the sources of interest marked. It can be seen they are in a reasonably uncluttered part of the diagram allowing them to be isolated. Furthermore, there are no 'holes' in the area of interest indicating that there is no areas of high extinction. Figure 2 shows the differential counts for the selected colour along with the Besançon model (Robin et al. 2003) for these stars. This model is widely used and generally accurately predicts the counts over wide areas of the sky. Here we have only run the model for the stars between F9V and G4V. The model was run with no extinction and predicted counts in $V$ which were then converted to $g$ using the $g - V$ colour for these stars. The Poissonian error bars from the counts in each magnitude bin is also shown.

The counts have two clear peaks, one at about $m_g = 17$ and a second at $m_g = 20.7$ with a minimum at $m_g = 19.5$ (see Fig. 2). This is seen most clearly at $b = 21^\circ$, and $b = 31^\circ$, however
even in the region $l = 180^\circ, b = 11^\circ$ there is some evidence for excess counts. The Besançon model does give a good fit to the data for $m_g < 18$, however, at $m_g = 20$ there is a sharp rise in the counts which is not predicted by the model. The peak corresponds with a distance of about 15 kpc from the Sun or a $R = 23$ kpc. This second peak cannot be caused by the halo, which is included in the model Besançon as the peak for these counts is predicted to start at $m_g \approx 23$ and reach a peak at about $m_g = 25$. Therefore, there are two possible alternatives; this is part of the disc or an extra galactic component, such as a stream beyond the disc of the Galaxy.

5. Analysis

These star counts cannot be produced by a simple exponential disc, even when including both the thin and thick disc, as such a model cannot produce this second bump (see figure 2). Even if there were no cut off this would only slightly affect the counts. However, a flared disc with no cut off may produce the second peak along specific lines of sight, as it would on average distribute stars
away from the plane. In order to explore this possibility, Eq. (1) has been used directly determine
the stellar density with distance assuming that the luminosity function can be replaced by a delta
function with \( M_b = 4.80 \). Figure 3 shows the density with galacto-centric radius for the lines of
sight far, and hence the contribution of the thin disc to the counts where the flare is important is
negligible. Therefore, this paper is only analysing the effect of the flare on the thick disc. Lines of
sight far closer to the plane would be required in order to analyse the effect of the flare in the thin
disc, and only then can any relationship between the flare in the thick and thin discs determined.

It was also assumed that the total number of stars at a galacto-centric radius followed a simple
exponential model. If this is not done then the large scale height caused by the flare would lead to
there being more stars in total at that galacto-centric radius.

The variation of stellar density is given by

\[
\rho = \rho_{\text{thin}} + \rho_{\text{thick}} + \rho_{\text{halo}},
\]

\[
\rho_{\text{thin}} = A \left( \frac{h_{z,\text{thin}}}{h_{z,\text{thin}}(R)} \right) \exp \left( \frac{R - R_\odot}{h_{R,\text{thin}}} \right) \exp \left( - \frac{|z|}{h_{z,\text{thin}}(R)} \right),
\]

\[
\rho_{\text{thick}} = 0.09 A \left( \frac{h_{z,\text{thick}}}{h_{z,\text{thick}}(R)} \right) \exp \left( \frac{R - R_\odot}{h_{R,\text{thick}}} \right) \exp \left( - \frac{|z|}{h_{z,\text{thick}}(R)} \right),
\]

\[
\rho_{\text{halo}} = 1.4 \times 10^{-3} A \exp \left[ \frac{10.093 \left( 1 - (\frac{R_{sp}}{R_\odot})^{1/4} \right)}{(R_{sp}/R_\odot)^{1/8}} \right],
\]

\[
h_{z,\text{thin/thick}}(R) = \begin{cases} h_{z,\text{thin/thick}}(R_\odot), & R \leq 16 \text{ kpc} \\ h_{z,\text{thin/thick}}(R) \exp \left( \frac{R - 16 \text{ kpc}}{h_r} \right), & R > 16 \text{ kpc} \end{cases}
\]

\[
R_{sp} = \sqrt{R^2 + 2.52z^2}
\]

This is, therefore, the standard thin and thick exponential disc model, but with a flare starting
at a specific galacto-centric radius. There are only two free parameters, the position of the start of
the flare and the scale length of the flare.

It should be noted that the aim is not to try and fit the model to the data but to demonstrate
that a simple model does reproduce the counts. Effects such as errors in the extinction calculation,
residual effects or the warp and the expected none axi-symmetry of the outer disc would be require a far more complex model and a far larger coverage of sky, in particular closer to the plane.

In Figures 2 and 3 the effects of various flares starting at a galacto-centric radius of 16 kpc are shown. For Fig. 2 the amplitude $A$ has been normalised to the measured counts between $m_g$ of 16 and 19, which is well before the flare starts. In Fig. 3, however, the density has been normalized to the measured $\int_0^\infty \rho(r)dr$.

Fig. 4 takes the densities and determines by how much the disc would need to be flared at each galacto-centric radius to give the determined density. At the radius of the Sun the relative scale height is 1 and it remains constant until a $R$ of 16 kpc, at which point the scale height increases rapidly. It is true that the flare is not identical in each case, however they are very similar with a typical flare scale length of $4.5 \pm 1.5$ kpc (Fig 4). There are, however, a number of effects which have not been taken into account.

- The warp has been ignored here, but would mean that the average plane position would be above $b = 0$ in the in the $l = 150^\circ$ region and below $b = 0$ at $220^\circ$. In the region 10-18 degrees from the plane the counts the flare increases rapidly, and so a small error in the position of the plane would significantly reduce the counts at $l = 150^\circ b = 15$.
- The simple model used here assumes a circularly symmetric outer Galaxy. As here we are dealing with the thick disc at 6 to 7 scale lengths from the Galactic centre, then if there were a 10% change in scale length with Galactic longitude it would lead to a 50% change in counts.
- The model used here assumes that the parameters of the flare do not depend on Galatic longitude.
- The extinction model used here is very simplistic.

Finally it should be noted that the counts for most distant points are very low leading to a large scatter. When far more regions become available it will be possible to quantify these effects and so refine the results.

These results do show that the variation of the number of stars with galacto-centric distance is consistent with an exponential law out to over 20 kpc. There is also no evidence for either a major drop in counts just before the flare starts or a sudden jump in the counts. This means that the counts in the disc can be described by a single function to beyond 20 kpc.

These plots show that the simple flare model not only predicts that at 20 degrees from the plane that there should be two peaks in the star counts, but can reproduce the numbers of counts and form.

The alternative scenario is a ring of stars centred at $R = 23$ kpc, which is detected for $R > 16–17$ kpc (Conn et al. 2007). As this structure would only exists in the outer Galaxy, its parameters are not constrained to fit observations in the solar neighbourhood or elsewhere in the Galaxy. This means that there is a wide range of possible parameter space that can be explored and hence by adjusting the width and density, a ring can be made to fit second peak. However, this ring must start very close to the edge of the disc. If the inner part of the stream is more than 1 or 2 kpc from the edge of the disc then there would be a noticeable drop in the stellar density at that point. Conversely if it overlapped with the edge of the disc then there would be a jump in the density. Furthermore, the number of stars in the stream has to be very similar to those predicted for the disc with no cut off, otherwise none of the flared models would come close to reproducing the measured counts.
Finally the vertical distribution of the counts again has to mimic the flared disc model, and this is over more that 20 degrees in latitude which correspond to 3 to 4 kpc at an \( R \) of 15 to 20 kpc. Hence, if there is a stream it would have to have many characteristics which are identical to those predicted for a flared outer disc.

6. Discussion

That the disc of the Galaxy is flared is widely accepted and is particularly well studied in the HI (e.g., Kalberla et al. 2007). They also find that the flare becomes relevant at around \( R = 16 \) kpc and the disc continues to at least 23 kpc. There may be also a dependence of the scale height with the galactocentric azimuth, as observed in the gas too (Kalberla et al. 2007), and this lopsidedness could find an explanation on the non-axisymmetrical distribution of pressures in the outer disc (López-Corredoira & Betancort-Rijo 2009).

By, in effect, moving sources away from the plane the result is that once the flare starts there will be a sharp drop in the counts when compared to the predictions of a simple exponential disc for any lines of sight near the plane, whereas at higher latitudes there will be considerably more stars than predicted. The sudden loss of stars beyond about \( R = 14 \) kpc is reported in Robin et al. (1992) when looking at \( l = 179^\circ \) \( b = -2.5^\circ \), and the results shown here shows that the second peak in the differential star counts at \( b = 20^\circ \) is entirely consistent with a flare.

The stars that are in the second peak would belong to the thick disc as they are typically 3 to 4 kpc above the plane and are at two to three times the galactocentric radius of the Sun. Their metallicity has been measured to be an average of \( [\text{Fe}/\text{H}] = -0.96 \), with an rms scatter of only \( \sim 0.15 \) dex (Ivezić et al. 2008), which is compatible with the metallicity of the outer thick disc (López-Corredoira et al. 2007, Fig. 3).

The flare of the thick disc is important for understanding its origin, as current theories suggest that thick discs caused by mergers will always flare. Bournaud et al. (2009) found that if a flare were caused by minor mergers then there would be no region of the thick disc with a constant scale height. The analysis presented here is not sensitive to changes in the scaleheight of thick disc closer to the solar circle as the counts for \( R < 16 \) kpc along the lines of site used are dominated by the thin disc. An analysis of the thick disc flare in the whole range of galactocentric distances would be necessary to see whether the mechanism proposed by Bournaud et al. (2009) is applicable here.

7. Conclusions

Uncertainties in our knowledge of the disc makes asserting the presence of the Monoceros stream principally because a model does not accurately reproduce the star counts dangerous, even when using a model as good as the Besançon model. If the disc has a cut off at \( R \) of about 14 kpc, as used in the Besançon model, then the ring would be necessary to give the star counts detected. If, however, there is no cut off and the thick disc instead flares, then the bulk of the stars in the regions being discussed here cannot belong to a stream as there are only sufficient stars to be explained by the disc alone. It should be noted that this would not preclude there being smaller scale streams towards the anti-centre affecting smaller regions of sky.

We have shown that a flare in the thick disc would leave a very clear signature in the star counts in the outer Galaxy, and that this signature is seen. We have shown that both the form and number
Fig. 4. The proportional flare in the scale height required to give the counts at each magnitude along each line of sight. The error bars from the number of sources detected in each magnitude bin are shown for one region.

of stars detected towards the anti-centre between 11 and 31 degrees from the plane can be readily explained by a flared thick disc without a cut-off. When a larger area of sky becomes available it will be possible to refine the outer disc and flare models and so improve the quality of the fit, in particular nearer the plane. Hence, the presence of the extra-galactic Monoceros ring/stream is not required to explain the star counts.

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References

Abazajian, K. N., Adelman-McCarthy, J. K., Agüeros, M. A., et al. 2009, ApJS, 182, 543

Bellazzini, M., Ibata, R., Martin, N., Lewis, G. F., Conn, B., & Irwin, M. J. 2006, MNRAS, 366, 865

Bilir, S., Cabrera-Lavers, A., Karaali, S., Ak, S., Yaz, E., & López-Corredoira, M. 2008, PASA, 25, 69

Bournaud, F, Elmegreen, B. G., & Martig, M. 2009, ApJ, 707, L1

Butler, D. J., Martínez-Delgado, D., Rix, H.-W., Peñarrubia, J., & de Jong, J. T. A., 2007, AJ, 133, 2274

Conn, B. C., Lewis, G. F., Irwin, M. J., Ibata, R. A., Ferguson, A. M. N., Tanvir, N., Irwin, J. M., 2005, MNRAS, 362, 475

Conn, B. C., Lane, R. R., Lewis, G. F., et al. 2007, MNRAS 376, 939

Conn, B. C., Lane, R. R., Lewis, G. F., Irwin, M. J., Ibata, R. A., Martin, N. F., Bellazzini, M., & Tuntsov, A. V. 2008, MNRAS, 390, 1388

de Jong, J. T. A., Butler, D. J., Rix, H.-W., Dolphin, A. E., Martínez-Delgado, D. 2007, ApJ 662, 259

Gilmore, G. & Reid, N. 1983, MNRAS, 202, 1025

Hammersley, P. L., Garzón, F., Mahoney, T., & Calbet, X. 1995, MNRAS, 273, 206
Ibata, R. A., Gilmore, G., & Irwin, M. J. 1994, Nature, 370, 194
Ivezić, Z., Sesar, B., Jurić, M., et al. 2008, ApJ, 684, 287
Kalberla, P. M. W., Dedes, L., Kerp, J., & Haud, U. 2007, A&A, 469, 511
López-Corredoira, M., 2006, MNRAS 369, 1911
López-Corredoira, M., Cabrera-Lavers, A., Garzón, F., & Hammersley, P. L., 2002, A&A 394, 883
López-Corredoira, M., Momany, Y., Zaggia, S., & Cabrera-Lavers, A. 2007, A&A 472, L47
López-Corredoira, M. & Betancort-Rijo, J. 2009, A&A, 493, L9
Martin, N. F., Ibata, R. A., Bellazzini, M., Irwin, M. J., Lewis, G. F., & Dehnen, W. 2004, MNRAS, 348, 12
Martínez-Delgado, D., Butler, D. J., Rix, H.-W., Franco, V. I., Peñarrubia, J., Alfaro, E. J., & Dinescu, D. I. 2005, ApJ, 633, 205
Momany, Y., Zaggia, S. R., Bonifacio, P., Piotto, G., De Angeli, F., Bedin, L. R., & Carraro, G. 2004, A&A 421, L29
Momany, Y., Zaggia, S. R., Gilmore, G., Piotto, G., Carraro, G., Bedin, L. R., & De Angeli, F. 2006, A&A 451, 515
Newberg, H. J., Yanny, B., Rockosi, C., et al. 2002, ApJ, 569, 245
Robin, A. C., Creze, M., & Mohan, V. 1992, ApJ, 400, L25
Robin, A. C., Reylé, C., Derrière, S., & Picaud, S. 2003, A&A, 409, 523
Rocha-Pinto, H. J., Majewski, S. R., Skrutskie, M. F., & Crane, J. D. 2003, ApJ, 594, L115
Schlegel, D. J., Finkbeiner, D. P., & Davis, M. 1998, ApJ, 500, 525