Probing gluon number density with electron-dijet correlations at EIC

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Abstract We propose a novel way of studying the gluon number density (the so-called Weizsäcker–Williams gluon distribution) using the planned Electron Ion Collider. Namely, with the help of the azimuthal correlations between the total transverse momentum of the dijet system and the scattered electron, we examine an interplay between the effect of the soft gluon emissions (the Sudakov form factor) and the gluon saturation effects. The kinematic cuts are chosen such that the dijet system is produced in the forward direction in the laboratory frame, which provides an upper bound on the probed longitudinal fractions of the hadron momentum carried by scattered gluons. Further cuts enable us to use the factorization formalism that directly involves the unpolarized Weizsäcker–Williams gluon distribution. We find this observable to be very sensitive to the soft gluon emission and moderately sensitive to the gluon saturation.

1 Introduction

High energy deep inelastic scattering (DIS) of electrons and nuclei at the future electron ion collider (EIC) [1] will provide a unique opportunity to perform detailed studies of various aspects of Quantum Chromodynamics (QCD) [2]. Amongst them is a formation of nuclei in terms of QCD degrees of freedom and, in particular, the dynamics of strongly correlated gluon systems, which leads to emergence of the phenomenon of saturation [3,4].

An especially interesting part of the EIC program concerns jet production [5]. It will allow to study in more detail the internal structure of various hadronic targets, such as p, Pb, Au [6,7], jet shapes, transport properties of cold nuclear matter [8] low x effects including gluon saturation [9], effects which are not all accessible in inclusive processes. As it has been recognized already in HERA-related studies [10–15] (see also [16]), the most suitable processes for the low x studies are those in which jets are produced in the forward direction with respect to the incoming electron, that is they have large rapidities. Kinematically, this allows for a better focus on the events in which the partons extracted from the proton or nucleus carry longitudinal momentum fraction, x, which is small enough for the saturation physics to be applicable and tested with high precision.

In the present, work we focus on the production of at least two jets in DIS collisions. Such processes are especially interesting, because, unlike inclusive processes, at high energies, they are directly sensitive to the gluon number density in hadrons, the so-called Weizsäcker–Williams transverse momentum dependent (TMD) gluon distribution [17,18].

The forward dijet production setup can be used reliably only if our theoretical predictions for that process reach certain quality. Specifically, the above kinematic configuration leads to appearance of two groups of potentially large logarithms: ln x and ln μ, where the latter, with μ being of the order of the transverse momenta of the jets, are called the Sudakov logarithms. Both types of logarithms should be resummed simultaneously and such resummation can be performed, as shown in Refs. [19,20], where the results were obtained in position space, using the color dipole formalism [21].

In this work we apply the recently formulated small-x Improved Transverse Momentum Dependent (ITMD) factorization [22,23] which generalizes the small-x TMD factorization [18] to account for power corrections, so that it reduces to the ordinary kT factorization [24] when the saturation effects are neglected. This framework, together with a model for the Sudakov resummation, has recently been successfully applied to shape description of dijet azimuthal angle decorrelations data in p − p and p − Pb collisions [25]. ITMD can be regarded as a special case of the Color Glass Condensate (CGC) [26] description once one neglects multiple partonic interactions (the so-called genuine twists)
The higher genuine twists and the two-body contribution is rather subtle \cite{30,31} and is accessible in rather small transverse momentum domain. It follows, that the higher genuine twists are suppressed at large transverse momenta or photon virtualities, \( Q^2 \). Therefore the ITMD framework is ideally suited for inclusive dijets studies, provided suitable kinematic cuts are imposed. A further advantage of this formalism is that it operates directly in momentum space and therefore allows to relax kinematic approximations often used in the coordinate space calculations. This is especially important for Monte Carlo implementations, which, in particular, allow for a very natural and flexible application of cuts.

In this letter we propose to utilize the azimuthal correlations between the forward dijet system and the scattered electron at EIC as a tool to study the gluon number distribution. This observable has not been studied in detail in the context of the saturation physics so far. Since there are three tagged final states – the scattered electron and two jets – there is a variety of potentially interesting observables. In studies of the TMD gluon distributions, especially in the saturation regime, the most interesting observables concern azimuthal correlations between the collision products. A quite standard choice is to look at the azimuthal angle between the jets \cite{23,32–35} or hadrons \cite{36,37}. It is obviously the only choice for the dijets at LHC, whereas for the DIS processes, one typically decouples the photon flux from the electron, and thus such observable seems also quite natural. However, in the approaches involving the TMD parton distributions, the transverse momenta of gluons extracted from the proton or nuclei (both internal and due to Sudakov-like soft emissions) are balanced by the whole final state, including the electron. As will be demonstrated in the following sections, the angle between the dijet system and the electron is very sensitive to soft gluon emissions and visibly sensitive to saturation effects. Hence, it offers a particularly good handle on quantifying the role Sudakov resummation in dijet production in DIS and its interplay with saturation effects. In general, observables involving scattered electron did not draw a lot of attention in the small-\(x\) community so far. Various asymmetries related to the EIC physics have been discussed on general ground in \cite{38}. Quite recently, in \cite{39} the Authors considered azimuthal electron-vector meson (or photon) correlations in exclusive diffractive production within CGC framework.

### 2 Framework

We consider the process of production of a dijet system in DIS

\[
e + h \rightarrow e' + J_1 + J_2 + X,
\]

where \( h \) can be a proton or an ion. The corresponding diagram is depicted on the left of Fig. 1, where we also define momenta of the particles involved in the process.

In our calculations, we shall use the ITMD framework, which, as explained in the Introduction, is suitable for our process of interest. It accounts for a complete kinematical twist, which amounts to resumming the \((Q_s/\vec{k}_T)^n\) and \((k_T^2/\vec{p}_T^2)^n\) contributions, where \( \vec{p}_T \sim p_{T1}, p_{T2} \), which has been shown by a derivation within CGC \cite{27}. Consequently, the offshellness of the initial-state gluon enters both into the TMD gluon density and to the hard matrix element. This observable has not been studied in detail in the context of the saturation physics so far. Since there are three tagged final states – the scattered electron and two jets – there is a variety of potentially interesting observables. In studies of the TMD gluon distributions, especially in the saturation regime, the most interesting observables concern azimuthal correlations between the collision products. A quite standard choice is to look at the azimuthal angle between the jets \cite{23,32–35} or hadrons \cite{36,37}. It is obviously the only choice for the dijets at LHC, whereas for the DIS processes, one typically decouples the photon flux from the electron, and thus such observable seems also quite natural. However, in the approaches involving the TMD parton distributions, the transverse momenta of gluons extracted from the proton or nuclei (both internal and due to Sudakov-like soft emissions) are balanced by the whole final state, including the electron. As will be demonstrated in the following sections, the angle between the dijet system and the electron is very sensitive to soft gluon emissions and visibly sensitive to saturation effects. Hence, it offers a particularly good handle on quantifying the role Sudakov resummation in dijet production in DIS and its interplay with saturation effects. In general, observables involving scattered electron did not draw a lot of attention in the small-\(x\) community so far. Various asymmetries related to the EIC physics have been discussed on general ground in \cite{38}. Quite recently, in \cite{39} the Authors considered azimuthal electron-vector meson (or photon) correlations in exclusive diffractive production within CGC framework.

\[
\frac{d\sigma_{eh \rightarrow e' + 2j + X}}{dx} = \int \frac{d^2k_T}{\pi} \frac{F^{(3)}_{gg}(x, k_T, \mu)}{4xP_e \cdot P_h} \times d\Phi(P_e, k; p_{e', p_1, p_2}) |\mathcal{M}_{eg \rightarrow e' + 2j}|^2,
\]

where the momenta are denoted such that \( P_h^\mu \) refers to the initial-state hadron, \( P_e^\mu \) to initial-state electron, \( xP_h^\mu + k_T^\mu \) to the initial-state space-like gluon, \( p_{e'}^\mu \) to the final-state electron, and \( p_{1,2}^\mu \) to the final-state partons, see Fig. 1. The differential phase space element is given by

\[
d\Phi(P_e, k; p_{e'}, p_1, p_2) = (2\pi)^{-2}d^4p_{e}d\delta_+(p_{e}^2)d^4p_1d\delta_+(p_1^2)d^4p_2d\delta_+(p_2^2)|\mathcal{M}|^2,
\]

so the electrons are assumed to be massless. In the above, the momentum of the off-shell gluon is given by \( k_T^\mu = xP_h^\mu + k_T^\mu \), with longitudinal momentum fraction \( x \) of nucleus \( P_h^\mu \) and transverse momentum such that \( P_h \cdot k_T = 0 \). \( |\mathcal{M}|^2 \) is the square of the parton-level scattering amplitude summed over spins and colors of the final-state electron and partons and averaged over the initial-state electron spins and gluon colors. Furthermore, it is summed over the allowed flavors of final-state partons. \( F^{(3)}_{gg}(x, k_T, \mu) \) is the hard-scale-dependent Weizsäcker–Williams (WW) unpolarized gluon density, counting the number of gluons at resolution scale \( \mu \).
It is given by

\[ F_{gg}^{(3)}(x, k_T, \mu) = \int db_T dk_T^2 \, b_T k_T^2 \, J_0(b_T \mu) \times J_0(b_T \mu) \, F_{gg}^{(3)}(x, k_T^2) \, e^{-S_{\text{Sud}}^q(q^2, \mu, b_T)}, \]

where

\[ F_{gg}^{(3)}(x, k_T^2) = 2 \int \frac{d\xi^+ d\xi^-}{(2\pi)^3 P_h^+} e^{i x P_h^+ + i k_T \xi} \times \langle P_h | F^{++}(\xi^-) | U^{[-i]} F^{++}(0, 0) | U^{[i]} P_h \rangle, \]

is the WW gluon distribution defined in terms of the matrix element of gluon field strength tensor components \( F^{++} \), displaced in the light cone and the transverse directions [45]. \( U^{[i]} \) are future-pointing gauge links, which make the gluon TMD gauge-invariant. The hard scale dependence of (4) comes from the Sudakov form factor, which itself is a process-dependent object. For dijet production in DIS, the Sudakov at the leading logarithmic approximation and with fixed coupling takes the form [19]

\[ S_{\text{Sud}}^g(q^2, \mu, b_T) = \frac{\alpha_s N_c}{4\pi} \ln^2 \frac{\mu^2 b_T^2}{4e^{-2\gamma_E}}, \]

where, in this work, we take \( \alpha_s = 0.2 \).

By using the above gluon density with appropriate evolution (see below) in the cross section formula (2) we achieve simultaneous resummation of small-\( x \) and the Sudakov logarithms. The former are relevant because by imposing the appropriate cuts, i.e. selecting the forward jets, we focus the probed longitudinal fractions \( x \) on its relatively small values. The latter appear because the production of relatively hard jets introduces additional logarithmic enhancements of the form \( \ln \left( \frac{p_T^2}{k_T^2} \right) \), which should be resummed. As mentioned above, the factorization formula (2) does not account for the linearly polarized gluons in the unpolarized hadrons. Since we are interested exclusively in the unpolarized WW gluon distributions and the related Sudakov resummation, we shall impose a rather low \( Q^2 \) cut, so that \( Q^2 / p_T^2 \) remains small and thus suppresses the linearly polarized gluon contributions. Even though it is possible to retrieve the linearly polarized part from the CGC formulation (see [31,44]), it is important to be able to test separate components of the calculation.

The WW gluon density can be obtained as a direct solution of the Balitsky–Jalilian–Marian–Iancu–McLerran–Weigert–Leonidov–Kovner (B-JIMWLK) evolution equation [46–54] or, assuming a Gaussian approximation, it can be constructed from the dipole gluon density obeying the Balitsky–Kovchegov (BK) equation [46,55]. In this paper we choose the latter option since the higher order corrections are better understood for the BK equation and are expected to be more relevant than the simplification due to the Gaussian approximation. Using that, we compute the gluon density from the solution of the BK equation with higher order corrections according to prescription of Kwieciński, Martin and Stašo (KMS) [56,57] yielding the Kutak–Sapeta (KS) gluon density [35] fitted to the proton’s \( F_2 \) structure function data. The momentum-space formulation of the BK equation allows us to treat the kinematics exactly. Therefore, the \( x \) variable appearing in the formula above is not the Bjorken \( x_B \) = \( Q^2 / 2P_h \cdot q \), but the actual fraction of the hadron momentum carried by the scattering gluon, and these two can differ significantly. Within the Gaussian approximation, one derives the following formula for the WW gluon density [23]

\[ F_{gg}^{(3)}(x, k_T) = \frac{2\pi^2 \alpha_s}{N_c k_T^2 S_{\perp}} \int \frac{d k_T^2}{2} \ln \frac{k_T^2}{k_T^2} \times \int \frac{d^2 q_T}{q_T^2} F_{gg}^{(1)}(x, q_T) F_{gg}^{(1)}(x, k_T - q_T), \]

where \( F_{gg}^{(1)} \) is the dipole gluon density and \( S_{\perp} \) is the target’s transverse area.

In Fig. 2 we show the WW KS gluon distributions in proton (left) and lead (right), with and without Sudakov form factors, as functions of the transverse momentum \( k_T \) and the hard scale \( \mu \), for one particular \( x = 10^{-3} \). (The gluon density is available from the TMDlib [58].) First of all, let us notice that the WW gluon distribution has no maximum, contrary to the dipole gluon [23,35]. Secondly, we see that the Sudakov factor suppresses the gluon distribution at low \( k_T \) and enhances it at higher \( k_T \). Because the Sudakov form factor is derived in the regime \( \mu \propto p_T \gg k_T \), we apply it.
only to that part of the gluon density where $\mu > k_T$. In the remaining domain, we use the gluon without Sudakov, given in Eq. (7). This is visible in Fig. 2 as a kink of the curve corresponding to $\mu = 17$ GeV. (A similar kink exits also for the $\mu = 67$ GeV curve but it is located at larger values of $\log k_T^2$.)

### 3 Results

In this section we present numerical results for the differential cross section as a function of the azimuthal angle between the total transverse momentum of the dijet system and the transverse momentum of the scattered electron, see the right plot of Fig. 1. The calculations are performed both for the $e^- p$ and $e^- Pb$ collisions at the center of mass (CM) energy $\sqrt{S} = 90 \text{ GeV}$ per nucleon. We look at low-virtuality events, with $Q^2 > 1 \text{ GeV}^2$, with inelasticity $0.1 < \nu < 0.85$. The final-state partons are subject to a jet algorithm, which, at leading order, is simply the cut on the azimuthal angle-rapidity plane, i.e. the requirement that $\sqrt{\Delta \Phi^2 + \Delta y^2} < R$. We choose the jet radius $R = 1$, as suggested e.g. in Ref. [5]. The jet definition is imposed in the Breit frame. Furthermore, we require that the transverse momenta of the jets satisfy $p_{T1} > p_{T2} > 3 \text{ GeV}$ in the Breit frame. In order to have a quite narrow distribution of the longitudinal fraction $x$, we select events with the laboratory (LAB) frame rapidities $-4 < y_1, y_2 < -1$, where the negative rapidity correspond to the incoming electron beam. The reason for this is illustrated in Fig. 3, where we show density plots for the gluon's $x$ versus the rapidity difference $y_1 - y_2$, for the above asymmetric cut (left) versus the symmetric cut $-4 < y_1, y_2 < +4$ (right). We see that the asymmetric cut gives us a very good focusing of the cross section around smaller values of the gluon $x \sim 0.008$. Note, that this corresponds to quite low Bjorken $x_{Bj} \lesssim 10^{-4}$. On the contrary, the symmetric cut provides a rather broad distribution in the gluon’s $x$, extending towards large values, where the formalism is questionable. To summarize, we impose the following cuts:

\begin{align*}
\sqrt{S} = 90 \text{ GeV}, \quad Q^2 > 1 \text{ GeV}^2, \quad 0.1 < \nu < 0.85 \\
\Delta R^{\text{Breit}} < 1, \quad p_{T1}^{\text{Breit}} > p_{T2}^{\text{Breit}} > 3 \text{ GeV}, \\
-4 < y_1^{\text{lab}}, y_2^{\text{lab}} < -1.
\end{align*}

(8)
Fig. 4 Azimuthal correlations between the total transverse momentum of the dijet system and the transverse momentum of the scattered electron at EIC in two frames: the LAB frame (left), the Breit frame (right). The calculation has been done within the ITMD* framework with the Weizsäcker–Williams gluon distribution obtained from the Kutak–Sapeta fit to HERA data.

We generate events using the KaTie [59] Monte Carlo and present our results both in the laboratory (LAB) frame and the Breit frame. The second option is a preferred choice for dijet observables since it suppresses the LO contributions, i.e. processes dominated by a quark jet [6].

As explained in the previous section, the selection choice (8), with $p_T$’s of jets larger than the $Q_s$, is motivated by our goal to study the Sudakov resummation effects together with the kinematical twist [27], in addition to the saturation effects, which, although rather mild, are expected to be present. In other words, the genuine twist configurations (i.e. multiple exchanges of non-soft gluons between the remnant and dijets [29]) as well as contributions from linearly polarized gluons [43] are suppressed. For the latter, we do not impose an upper cut on $Q^2$ as the cross section is strongly peaked at low virtualities and such additional cut would introduce only a small correction.

Our predictions for the cross section as a function of the angle between electron and dijet system are presented in Fig. 4. We plot also a control result based on a calculation that neglects the Sudakov form factor. The comparison of the two results clearly shows that while saturation effects are mild, the Sudakov effects are fairly large. This feature is clearly visible in both the LAB and the Breit frame. In the LAB frame the difference is concentrated around the correlation region of the dijet-electron system. In the Breit frame, on the other hand, the Sudakov form factor suppresses the cross section over the whole region of the azimuthal angle. Let us note, that the Breit frame is defined in a standard way in our calculation, that is by requiring the photon to have nonzero only the spatial $z$ component. However, unlike in collinear factorization, there is a non-zero transverse momentum of the incoming parton in the factorization formula (2), which makes this frame slightly less intuitive. The saturation effects are observed as an almost constant suppression of the electron-lead cross section (normalized to the number of nucleons) over all azimuthal angles. The suppression reaches maximally about 15%, which although modest, is an observable effect. To be so, the jets must have relatively small $p_T \sim 3$ GeV in Breit frame, thus, in practice, one can consider dihadron-electron correlations.
4 Conclusions

In this Letter we proposed a new study of the Weizsäcker–Williams gluon distribution, using the azimuthal correlations between the forward dijet system and the scattered electron at the EIC. We chose the kinematic cuts such that both the genuine twists and the linearly polarized gluons are suppressed. This gives us a direct access to the unpolarized distribution via the small-$x$ ITMD factorization. We provided predictions over whole range of the azimuthal angle, which is possible thanks to the inclusion of the kinematic twists and full phase space.

We found that forward dijet-electron azimuthal correlations provide a more sensitive observable to the Sudakov suppression, shown in Fig. 4, as compared to the jet-jet correlations alone, depicted in Fig. 5. In the latter case the difference is concentrated in the region very close to the correlation peak (in Breit frame), whereas for the former observable it extends over large region of azimuthal angle.

Our results may serve as a guidance for future measurements at EIC and improved calculations at the NLO accuracy.

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