PHOTONICS

Direct imaging of isofrequency contours in photonic structures

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The isofrequency contours of a photonic crystal are important for predicting and understanding exotic optical phenomena that are not apparent from high-symmetry band structure visualizations. We demonstrate a method to directly visualize the isofrequency contours of high-quality photonic crystal slabs that show quantitatively good agreement with numerical results throughout the visible spectrum. Our technique relies on resonance-enhanced photon scattering from generic fabrication disorder and surface roughness, so it can be applied to general photonic and plasmonic crystals or even quasi-crystals. We also present an analytical model of the scattering process, which explains the observation of isofrequency contours in our technique. Furthermore, the isofrequency contours provide information about the characteristics of the disorder and therefore serve as a feedback tool to improve fabrication processes.

INTRODUCTION

Although band structures are useful for understanding and predicting the optical properties of photonic crystal (PhC) slabs, they are typically calculated or measured only along high-symmetry directions because of computation and time constraints. A more comprehensive understanding of a PhC slab lies in its isofrequency contours: slices in two-dimensional (2D) momentum space ($k_x$, $k_y$) of constant frequency $\omega$. In particular, isofrequency contours are essential for understanding phenomena that depend on the direction of group velocities, such as negative refraction (1), supercollimation (2, 3), and superlensing (4). In recent years, the full dispersion of radiative PhC slab resonances has gained further interest for their important roles in topics including non-Hermitian physics (5–7), bound states in the continuum (8, 9), zero-index metamaterials (10, 11), lasers (12), sensors (13), coherent perfect absorbers (14, 15), solar cells (16), radiative cooling (17, 18), and structural color (19). However, obtaining isofrequency contours is not trivial, and current experimental techniques involve samples with strong disorder (20). To demonstrate this technique, we fabricated a hole-array PhC slab with a thickness of 180 nm on top of a SiO2 substrate. The sample slab was fabricated using interference lithography (23). Fourier plane microscopy is another widely used method (24–28) and can provide isofrequency contours inside or outside the light cone, yet the use of mode-coupled fluorescence directly limits the accessible wavelength range. These methods have been applied to photonic resonances in dielectric structures (20, 21, 23), as well as to plasmonic resonances in metallic structures (22, 24–31).

As an alternative, we demonstrate direct imaging of isofrequency contours using resonance-enhanced photon scattering arising from minimal, intrinsic fabrication disorder in a “pristine” sample. The experimental isofrequency contours show good quantitative agreement with numerical results throughout the visible wavelength regime. To understand the underlying physical process, we use temporal coupled-mode theory (TCMT) (32–34) to show that scattering is enhanced for on-resonance photons and that the angular distribution of scattered photons recreates the isofrequency contours in the far field. Intrinsic disorder (35) and resonance-enhanced scattering (36–38) have been used to study localized photonic modes, but we show that this scattering process can also be used to probe large-area, delocalized resonances and their corresponding isofrequency contours. Additionally, our results reflect information about the characteristic fabrication disorder in a PhC slab and thus serve as a feedback method for improving the fabrication processes. This technique may also be extended to quasi-crystals and may provide an experimental route to obtain their isofrequency contours, which are quite challenging to obtain using current numerical tools.

RESULTS

Direct imaging of isofrequency contours

The direct imaging mechanism relies on a simple process (Fig. 1A). We excite a PhC slab resonance using incident light at the proper frequency $\omega$ and in-plane wavevector ($k_x$, $k_y$). The natural disorder in the sample scatters light in this resonance to resonances at other wavevectors, depending on the spatial Fourier coefficients of the fabrication disorder. These resonances then radiate photons, which recreate the isofrequency contour in the far field. By scanning the frequency of the light source and tuning the incident angle accordingly, we can visualize isofrequency contours throughout the visible spectrum. A quantitative description of the resonance-enhanced scattering process is presented in the next section.

To demonstrate this technique, we fabricated a hole-array PhC slab and observed the distribution of scattered photons. A large-area PhC slab was fabricated using interference lithography (39). As shown in Fig. 1B, a high-quality square lattice of cylindrical air holes with a radius of 103 nm and a periodicity of 336 nm was patterned into a Si3N4 slab with a thickness of 180 nm on top of a SiO2 substrate. The sample was then mounted in a cell filled with liquid of refractive index $n_{\text{liquid}} = 1.46$, which was then placed on a rotation stage (Newport) for precise control over the incident angle (Fig. 1C). Because we use liquid with the same refractive index as the SiO2 substrate, our sample has an up-down mirror symmetry, and thus, we can separate the resonances into transverse magnetic-like (TM-like; odd-in-z) and transverse electric-like (TE-like; even-in-z) modes. The sample was then excited with a broadband supercontinuum source (SuperK, NKT) through a narrow (10 nm) band-pass filter, as shown in Fig. 1C, or with a narrow-linewidth laser. A polarizer was placed along the beam path to allow selection between...
Resonance-enhanced scattering

To better understand the imaging technique, we present a theoretical treatment of the resonance-enhanced scattering process. It is well known that macroscopic optical resonances can be used to trap light and therefore enhance nonradiative processes, like optical absorption. This leads to intriguing physical phenomena, such as coherent perfect absorption (41, 42), critically coupled resonators (43), and complete photon absorption in a graphene monolayer (11). However, the possibility of using large-area resonances to enhance scattering remains largely unstudied. In this section, we consider a general PhC slab and compute the enhancement of scattered light from intrinsic fabrication disorder and surface roughness under both on- and off-resonance conditions.

An effective tool to understand this process is TCMT (32–34). Consider a collimated beam incident on the PhC slab that excites a resonance. We treat the Rayleigh scattering from the disorder of the slab as a non-radiative decay channel for the resonance, because photons being scattered do not contribute to the power in the transmission and reflection channels, similar to photons being nonradiatively absorbed. For high-quality PhC slabs made of low-loss dielectrics, the decay channel for the resonances via material absorption is negligible (39, 44) compared to scattering. When the scattering is weak and the lifetime of the resonance is sufficiently long, we can approximate the total amount of scattered light as (32)

$$P_{\text{scat}} = \frac{2\gamma_r \gamma_{\text{scat}}}{(\omega - \omega_0)^2 + (\gamma_r + \gamma_{\text{scat}})^2}$$

where $P_{\text{scat}}$ is the scattered power, $P_{\text{in}}$ is the incident power, $\omega$ is the incoming photon frequency, $\omega_0$ is the resonance frequency, $\gamma_r$ is the radiative decay rate of the resonance, and $\gamma_{\text{scat}}$ is the decay rate due to scattering from disorder (section S1). Here, we consider only one resonance in the PhC slab, but the generalization into multiple resonances is straightforward. From Eq. 1, the scattering rate is most efficient ($P_{\text{scat}}/P_{\text{in}} = 50\%$) when the system is driven on resonance ($\omega = \omega_0$) and the radiative decay rate equals the scattering decay rate ($\gamma_r = \gamma_{\text{scat}}$). This result agrees with the well-known results in critical coupling for absorption enhancement (11, 43, 45). By engineering the quality of the resonances in a PhC, this technique can accommodate samples with different levels of disorder.

Next, we consider the angular distribution of the scattered photons, which leads to the formation of isofrequency contours in the far field. The resonance-enhanced scattering can be modeled as a three-step process (Fig. 1A). In the first step, incoming light with frequency $\omega$ excites a resonance at in-plane wavevector $k_{\text{in}}$. In the second step, disorder couples the resonance at $k_{\text{in}}$ to resonances at other wavevectors, $k_{\text{out}} \neq k_{\text{in}} + \Delta k$. The strength of this coupling depends on the spatial Fourier coefficient of the disorder at $\Delta k$, $|F_{\Delta k}|^2$. In the third step, resonances at $k_{\text{out}}$ radiate photons into the far field with outgoing angles specified by frequency $\omega$ and in-plane momentum $k_{\text{out}}$.

The photons acquire random phases through the disorder coupling (second step), so their subsequent reradiation (third step) can be modeled as the radiation from a collection of randomly polarized dipoles with number density of $N_0$ and dipole strength of $\mu$. As a result, the decay rate into the radiation channel with in-plane wavevector $k_{\text{out}}$ and frequency $\omega$ depends on the spectral density of states (46) in the vicinity of the PhC slabs and can therefore be approximated as

$$\Gamma(k_{\text{out}}, \omega) = \frac{N_0\pi\kappa|\mu|^2}{3\hbar}\sum_{n} \frac{1}{\pi} \left( \frac{\Delta\omega_{\text{scat}}^n}{(\omega - \omega_{\text{out}}^n)^2 + (\Delta\omega_{\text{scat}}^n)^2} \right)$$

Here, $\mu$ is the average electric dipole strength depending on the total power in the scattered photons, $n$ labels different PhC resonances at a...
Fig. 2. Direct visualization of isofrequency contours. (A) Numerical simulation (COMSOL) of band structure, with the colored vertical lines corresponding to wavelengths of the isofrequency contours below. TE-like bands are dashed and TM-like bands are solid. Numerical [MEEP for (B) to (E); COMSOL for (F) to (I)] and experimental isofrequency contours at (B) 488 nm, (C) 514 nm, (D) 532 nm, (E) 550 nm, (F) 580 nm, (G) 600 nm, (H) 610 nm, and (I) 620 nm. Note that the numerical and experimental contours are shown with different scales due to small, systematic differences in angles that can be avoided with a careful angle calibration and knowledge of the precise geometric parameters of the sample. TE-like contours are dashed and TM-like contours are solid. In all cases, the incident beam excited a TM-like resonance. The experimental data use incident light with s-polarization at angles of (B) −14.4°, (C) −8.0°, (D) −2.6°, (E) −5.6°, (F) −5.1°, (G) −9.8°, (H) −12.4°, and (I) −15.4°. The dark, horizontal line in the middle of the experimental contours is the slit in the screen for the incident and the specularly reflected beams to pass through.
Dw

given \( k_{\text{out}} \), \( \alpha_n \) represents the coupling between the initially excited resonance and the final resonance mediated by the surface roughness, \( \Delta \omega_{\text{out}} \), \( \omega_{\text{out}} \), and \( \omega_{\text{in}} \) are the linelengths of the outgoing resonances accounting for both radiative and nonradiative decay, and \( \omega_{\text{in}} \) are the central frequencies of the outgoing resonances (section S2). From Eq. 2, it is clear that scattering is maximized when the emission frequency is on-resonance with one of the resonance frequencies for a given momentum (\( \omega = \omega_{\text{out}} \)). Therefore, for incident light with frequency \( \omega_0 \), we expect large scattering for the momenta \( k_{\text{out}} \) that provide resonances also at \( \omega_0 \). Accordingly, the highest-intensity positions in the far field will correspond to the isofrequency contours of this PhC slab at the frequency of \( \omega_0 \).

To experimentally demonstrate that this technique relies on resonance-enhanced scattering, we measured the spectrum of the scattered photons from the PhC slab when excited with a supercontinuum source. We removed the paper screen in the experimental setup shown in Fig. 1C. Scattered photons were then collected using a lens with a numerical aperture (NA) of 0.25 and a focal length of 5 cm that was placed in front of a spectrometer with a spectral resolution of 0.03 nm (HR4000, Ocean Optics). The distance between the spectrometer and the lens was optimized to maximize the coupling of the scattered photons into the spectrometer. The positions of the spectrometer and the lens were fixed during the experiment, and the sample was rotated between 0° and 8° from the normal direction with a step size of 0.1°. Throughout this measurement, we ensured that the directly reflected beam was not captured by the lens, so only scattered light was recorded. We note that the two scattering measurements presented (Figs. 2 and 3) characterize different physical properties. For Fig. 2, the excitation source is a laser (or a narrow-band source) with a well-defined wavelength. Characterization of the angular distribution of the scattered photons leads to the isofrequency contours. On the other hand, for Fig. 3, the excitation source is a broadband supercontinuum. For detection, we do not distinguish between outgoing angles (by placing a lens with \( \text{NA} = 0.25 \) in front of the spectrometer) but instead only measure the spectrum of all scattered photons.

The experimental scattering spectra are shown in the middle column of Fig. 3. The scattering peaks show good quantitative agreement with the numerical results for the locations of the resonances obtained from COMSOL (shown in the left column). This can be understood from Eq. 1: the enhancement is maximized when the incident light frequency is on resonance. S- and p-polarized light excite different resonances due to symmetry: the incident beam and the structure are both mirror-symmetric in the \( y \) direction. Therefore, the even (odd) incident beam can only excite even (odd) resonances with respect to \( y \), as described by Hsu et al. (8) and Lee et al. (44). Exemplary line cuts of the scattering spectra at 4.3° are shown in the right column, which show that the experimental results agree well with the expected Lorentzian line shapes.

As we can see in Fig. 3, the resonance-enhanced scattering process is also an efficient way to measure PhC band structures, avoiding the shortcomings of other standard techniques. For example, reflection measurements are often used to measure band structures because Fano features in the spectrum indicate resonances (47). However, reflection measurements require constantly moving the spectrometer to maintain overlap with the specularly reflected beam. On the other hand, enhanced fluorescence measurements require additional incorporation of emitters and are limited by their emission bandwidth (48). Finally, enhanced absorption measurements inevitably lower the quality factors of the resonances because of the incorporation of a lossy medium (49). The method that we present takes advantage of minimal, generic fabrication errors and surface roughness in any high-quality resonator (for example, the resonances we measured have quality factors as high as \( Q \approx 5000 \), does not require moving the spectrometer, and allows for a fast and direct measurement of the resonance central frequencies and the quality factors.

**DISCUSSION**

The experimental isofrequency contours also give information about the characteristic fabrication errors in the PhC slab, which is not possible to obtain otherwise. As shown in Fig. 2, for a given frequency, the contours corresponding to TM-like resonances (solid lines) are significantly brighter than those corresponding to the TE-like resonances (dashed lines). This means that the disorder in our sample predominantly couples the initial incoming TM-like resonance to outgoing TM-like resonances (instead of TE-like resonances), which suggests that the major sources of fabrication errors also satisfy up-down mirror symmetry. Therefore, we know that the fabrication errors that do not break up-down mirror symmetry (for example, distortions of the hole shape in the interference process) dominate over those errors that break the up-down mirror symmetry (for example, oblique side walls in the etching process). Furthermore, we can determine the characteristic length scale of the disorder by analyzing the intensity of the isofrequency contours (section S3).

Additionally, resonance-enhanced scattering has applications in several display technologies. In particular, transparent displays have been realized using plasmonic resonances (50, 51), but the high-quality factors of photonic resonances, due to negligible absorption and narrow linewidths, may allow for significantly better performance. If the isofrequency contour is engineered to be at large angles and therefore

Fig. 3. Experimental verification of resonance-enhanced scattering. Numerically calculated band structure (left) and experimentally measured scattering spectrum (middle) for (A) s-polarized and (B) p-polarized light. The right column shows line cuts at 4.3° from the experimental scattering spectrum.
far away from a viewing audience, the resonance-enhanced scattering process can be used for a transparent display. A large portion of the ambient light will pass through the display, but light from a laser projector incident at resonant angles will be scattered and will form an image. Projecting incoming light of different polarization states or wavelengths could allow for a transparent 3D display. Furthermore, engineering isofrequency contours to direct photons to different angles could create a privacy screen. By projecting light at a specified incident angle, viewers at particular directions could see the strongly scattered light, whereas viewers at other angles can only see a transparent panel.

In conclusion, this article presents theoretical and experimental results on enhanced photon scattering in the presence of a large-area, nearly pristine PhC slab. We use this phenomenon to measure the band degeneracy in photonic crystals and zero-refractive-index materials. Nat. Mater. 10, 582–586 (2011).

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