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Precise Reactive Power-Voltage Droop Control of Parallel Virtual Synchronous Generators That Considers Line Impedance

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Abstract: Problems such as high power coupling, low distribution accuracy, and insufficient reactive power-voltage droop accuracy occur when distributed generators are operated in parallel due to the influence of line impedance. The precise control of output reactive power and voltage is difficult to achieve using traditional virtual synchronous generator (VSG) control. Taking this into consideration, this study proposes a virtual synchronous generator reactive-power-voltage integrated control strategy that considers line parameters to solve this problem. First, the impedance voltage drop of the line is compensated for in accordance with local information control to ensure the consistency of the control voltage in parallel operation of distributed generators and to realize the precise droop control of reactive power and the voltage at the point of common coupling ($U_{PCC}$). Second, virtual negative impedance control is added to change the equivalent output impedance characteristics of the system and achieve power decoupling. On this basis, the active frequency and reactive voltage decoupling control effect of the improved control strategy is quantified and analyzed using the relative gain matrix. The accuracy of reactive power distribution and droop control is theoretically derived and analyzed by establishing a small-signal model of a two-machine parallel system. Finally, the accuracy and effectiveness of the proposed integrated control strategy are verified via a simulation model and an experimental platform for parallel operation. Results show that the proposed integrated control strategy can effectively solve the problems of power decoupling and accurate distribution, reduce system loop current, and realize accurate reactive power-voltage droop. Compared with the traditional VSG control strategy, the dynamic deviation of $U_{PCC}$ is reduced by at least 40% when a large-scale load disturbance occurs.

Keywords: distributed microgrid; virtual synchronous generator; reactive power-sharing; accurate voltage control; relative gain matrix

1. Introduction

Microgrid technology has elicited considerable attention with the growing maturity of new energy generation technology. Microgrids contain distributed generators (DGs), energy storage units, converters, loads, and protection and control devices [1]. They can be connected to the main grid for grid-connected operation or isolated from it [2]. When a microgrid is in an island operation state, the control mode is divided into two types: master-slave control and peer-to-peer control [3]. Although the structure of master-slave control is simple, its disadvantages, such as poor system stability and high operation cost, cannot be disregarded and are not conducive for large-scale applications [4]. The peer-to-peer control mode can achieve independent control among different DGs and quickly complete load...
disturbance response without communication, considerably improving the reliability of the system power supply and the economy of the operation. Therefore, distributed microgrids with peer-to-peer control have become a research hotspot [5].

At present, distributed microgrids based on the peer-to-peer control mode adopt droop control for each distributed generation micro-source. However, considering the rapid development of microgrids, the operating characteristics of low inertia and underdamping cannot be disregarded. To improve the security and stability of microgrid operation, many scholars have proposed virtual synchronous generator (VSG) control [6]. Inertia and damping links are added based on droop control by simulating the external characteristics of a synchronous generator set. When load disturbance occurs, inertial support can be provided immediately to avoid the large-scale oscillation of a system [7].

Existing experiments and actual projects have verified the effectiveness of this control strategy [8]. However, the problem of accurate power allocation in a microgrid system when multiple DGs operate in parallel cannot be disregarded whether in droop control or VSG control. The output line impedance parameters of a system and the terminal control voltage cannot be matched due to the varying capacities and scattered locations among different DGs [9]. The power output of DGs is coupled, and the precise droop control of reactive power-voltage cannot be achieved. When power distribution deviation occurs in a system, circulating current is easy to produce, leading to an increase in system loss and affecting the power quality of a system.

Scholars have proposed various solutions to these problems based on the traditional VSG control [10–19]. The accuracy of the reactive power distribution of a system was improved by introducing virtual impedance control based on the analysis of power coupling in [10–12]. The virtual negative impedance control is introduced in [10]. By introducing the virtual impedance parameter to increase the inductance component of the system, the impedance parameter matching between different DGs is realized. In References [11,12], virtual positive impedance control is introduced to adjust the resistive component of equivalent output impedance. These methods can achieve power decoupling and ensure accurate power distribution. However, the introduction of virtual impedance will cause an excessive drop in the voltage of the point of common coupling (PCC) \(U_{\text{PCC}}\), degrading the power quality of a system. The reactive power-voltage control strategy based on adaptive virtual impedance, which is realized by adding adaptive disturbance to virtual impedance, was reported in [13]. This technique uses a synchronous communication system to complete information interaction. Ensuring that the receiving time of each DG is consistent is necessary and requires a real-time communication link. An adaptive impedance control based on a consistent control algorithm was proposed to further improve the accuracy of reactive power distribution further [14]. In References [15,16], a control strategy with low real-time requirements for communication was presented to reduce power output deviation through the coupling relationship among powers. However, the action time of the synchronization signal was difficult to determine. The quality of the terminal voltage was improved by directly applying \(U_{\text{PCC}}\) to the voltage feedback of a double-loop control system in [17]. This technique requires high accuracy of information transmission, and the delay in communication reduces the flexibility and stability of system control. Accurate reactive power allocation was achieved based on voltage droop control and bus voltage at PCC [18]. In References [2,19], the parameters of microgrid lines were used to modify the reactive power droop coefficient to achieve a reasonable reactive power distribution. Although these methods improve the power distribution accuracy of a system, the reactive power-voltage droop characteristic also changes.

In accordance with the analysis of the aforementioned control methods, current problems related to reactive power-voltage control caused by a difference in line impedance have not been resolved fully. Most control schemes focus on front-end reactive power distribution and the precise control of output voltage, and they highly depend on the stability of the communication link and the accuracy of information. The precise droop control effect of reactive power-voltage at the end of the line (i.e., the user side) and
the effect of local information are seldom considered. To realize the “plug-and-play” and precise reactive power-voltage droop control effect of parallel DGs, a VSG reactive power-voltage integrated control strategy that considers line parameters is proposed in the current study. Combined with local information control, the line impedance voltage drop is compensated for, and the control voltage is moved forward to the PCC. Notably, the integrated control not only realizes the precise distribution of reactive power by matching the control voltages of different DGs, but it also achieves precise droop control of the voltage at PCC ($U_{PCC}$). Simultaneously, power decoupling is achieved by introducing virtual negative impedance control to improve system dynamic performance. The output power decoupling control effect of the improved control strategy is quantified and compared with the first amplification factor matrix and the relative gain matrix. The small-signal model of a two-machine parallel system is developed to theoretically verify the deviation of reactive power distribution and the accuracy of reactive power-voltage droop control. Finally, the effectiveness of the proposed integrated control strategy is verified via simulation and an experimental platform.

2. Limitation Analysis of Traditional VSG Control

2.1. Traditional VSG Control

The VSG main circuit topology and control scheme adopted in the current study are illustrated in Figure 1. To simplify the analysis, the direct current (DC) side is replaced with a constant voltage source. The high-order harmonics of the voltage at the output side of the inverter bridge arm ($E_{abc}$) are eliminated using an LC filter to obtain the voltage at the output side of the VSG ($U_{abc}$). It supplies power to the public load at the PCC after the line impedance $Z_{line}$. $U_{dc}$ is the voltage of the DC-side voltage source; $C_{dc}$ is the capacitance value of the DC side; $i_{fabc}$ and $i_{abc}$ are the inductance current and VSG output current, respectively; $L$ is the filter reactance; and $C$ is the filter capacitor.

![Figure 1. Topology and control scheme of the VSG.](image_url)

The VSG control scheme includes an active frequency control loop, a reactive voltage control loop, a three-phase modulated wave generator, and a space vector pulse width modulation regulator. The mathematical expressions for the active frequency control loop and the reactive voltage control loop are given in (1)–(3).

\[
\frac{d\omega}{dt} = \frac{P_{ref}}{\omega_s} - \frac{P_e}{\omega_s} - D_p(\omega - \omega_s)
\]  

(1)
\[
\theta = \int \omega \cdot dt 
\] (2)

\[
K \frac{dE}{dt} = Q_{ref} - Q_e + D_q(E_0 - U_0) 
\] (3)

where \( P_{ref} \) and \( Q_{ref} \) are the given values of active and reactive power, respectively; \( P_e \) and \( Q_e \) are the instantaneous output active and reactive power, respectively, of the VSG through a low-pass filter; \( D_p \) and \( D_q \) are the droop coefficient of the active frequency and reactive voltage, respectively; \( \omega \) is the VSG output angular frequency; \( \omega_s \) is the system-rated angular frequency; \( E_0 \) is the rated output voltage amplitude; \( U_0 \) is the actual output voltage amplitude; \( J \) is the virtual moment of inertia; and \( K \) is the equivalent inertia coefficient.

2.2. Limitations of VSG Control Power Distribution

Using the parallel system of two VSGs as an example, the equivalent circuit diagram is shown in Figure 2. In the figure, \( E_i \) and \( \delta_i \) \((i = 1, 2)\) are the output amplitude and phase angle of the VSG equivalent voltage source. \( \delta_i \) is usually small, and it can be approximately regarded as \( \sin \delta_i = \delta_i \), \( \cos \delta_i = 1 \). \( U_{PCC} \) is the voltage amplitude of the PCC. \( Z_i \) is the equivalent output impedance, and \( \varphi_i \) is the equivalent output impedance angle. \( Z_0 \) is the load impedance. \( I_i, I_0, \) and \( I_{cc} \) are the VSG output current, load current, and system circulating current, respectively.

![Figure 2. Equivalent circuit diagram of two parallel VSGs.](image)

When the equivalent output impedance of a system is inductive (i.e., \( X_i > R_i \)), the equivalent output impedance angle \( \varphi_i = 90^\circ \) can be considered. At this moment, the expressions of the VSG single-phase output active power and reactive power are given in (4).

\[
\begin{align*}
P_{ei} &= \frac{E_{PCC}}{X_i} \delta_i \\
Q_{ei} &= \frac{U_{PCC}(E_i - U_{PCC})}{X_i}
\end{align*}
\] (4)

From the preceding equation, when the equivalent output impedance is inductive, the active and reactive power of a system are related to the phase angle \( \delta_i \) and voltage deviation \( (E_i - U_{PCC}) \), respectively. The output adjustment of VSG active power can be realized by adjusting the phase angle, and reactive power can be improved by adjusting voltage deviation, meeting the basic principle of VSG control.

In accordance with the VSG control equation, considering that frequency is a global variable, active power distribution in steady-state operation is only related to the given values of active power \( P_{ref} \) and droop coefficient \( D_p \), which are unaffected by system line parameters. However, the output voltage of a system is not a global variable and is closely related to line parameters. When differences exist in line parameters among DGs, reactive power cannot be distributed in accordance with the rated capacity [20]. In the traditional VSG reactive voltage control strategy, the setting of the droop coefficient \( D_q \) is closely related to the output reactive power of VSG and the voltage in the first section of the line. However, the droop coefficient deviation caused by line impedance voltage drop and power loss cannot be disregarded [21]. The precise droop control effect of reactive power-voltage at the end of the line (i.e., user side) should be given increased attention.
3. Integrated Control Strategy

3.1. Improved VSG Reactive Voltage Control

The current study proposes an improved control scheme of reactive voltage based on local information control quantity. The output voltage $U_0$ of the VSG in the reactive voltage control loop is compensated for by the line parameter voltage drop $\Delta U_{\text{line}}$ and converted into voltage at the public load $U_{\text{PCC}}$. It compensates for the voltage deviation caused by the difference in line impedance of various DGs and ensures the consistency of the control voltage. Simultaneously, precise droop control between reactive power and line terminal voltage is realized, and the public alternating current (AC) bus voltage is optimized, further satisfying the “plug-and-join” control requirements of different DGs.

The block diagram of the improved reactive voltage control of the VSG is shown in Figure 3.

![Figure 3. Block diagram of the improved reactive voltage control of the VSG.](image)

In the improved control strategy, the reactive power expression is given in (5) when a system is in steady-state operation.

$$Q_e = Q_{\text{ref}} + D_q(E_0 - (U_0 - \Delta U_{\text{line}}))$$

$$= Q_{\text{ref}} + D_q(E_0 - U_{\text{PCC}})$$

(5)

As shown in Figure 3 and (5), when line impedance $Z_{\text{line}}$ is added to the reactive voltage control loop, reactive power distribution is only related to the rated output voltage amplitude $E_0$ and the reactive droop coefficient $D_q$. The precise distribution of reactive power can be realized in steady-state, and voltage in the PCC at the end of the line can be controlled to enable it to work near the rated operating point. The problem of low $U_{\text{PCC}}$ caused by line impedance and virtual impedance can be avoided.

3.2. Virtual Negative Impedance Control

The traditional VSG control is designed when the equivalent output impedance is inductive. However, a distributed microgrid is in the low-voltage operation state, and its line parameters are typically resistive or resistive-inductive. Load power changes cause considerable power coupling and dynamic circulation, affecting the dynamic control performance of each DG and the accuracy of output power distribution [22].

To realize the decoupling of active and reactive power and independent control in the dynamic regulation process, many experts have introduced the control idea of “virtual negative impedance” [23,24]. The expression for the typical virtual negative impedance control in the Dq coordinate system is given in (6).

$$\begin{cases} E_{\text{ref},d}^* = E_{\text{ref},d} + R_v i_{od} - s L_v i_{od} + \omega_s L_v i_{oq} \\ E_{\text{ref},q}^* = E_{\text{ref},q} + R_v i_{oq} - s L_v i_{oq} - \omega_s L_v i_{od} \end{cases}$$

(6)

where $R_v$ and $L_v$ are the virtual resistance and virtual inductance values, respectively; $E_{\text{ref},d}$ and $E_{\text{ref},q}$ are the $d$-axis and $q$-axis components of the reactive voltage loop output reference voltage, respectively; $i_{od}$ and $i_{oq}$ are the $d$-axis and $q$-axis components of the
output current, respectively; and $E^*_{\text{ref},d}$ and $E^*_{\text{ref},q}$ are the references for the three-phase modulated wave generator after virtual impedance correction. The block diagram of the integrated control strategy is shown in Figure 4.

![Figure 4. Block diagram of the integrated control strategy.](image)

4. Analysis and Theoretical Verification of the Integrated Control Strategy Based on Relative Gain

To visually analyze the difference between the integrated control strategy and the traditional VSG control strategy in terms of power decoupling and the precise distribution of reactive power, the two parallel VSGs in Figure 2 are used as an example for analysis. First, the first amplification factor matrix and relative gain matrix [25] are introduced to quantitatively compare and analyze the decoupling control effects of the two different control strategies on the active frequency and reactive voltage. Second, the small-signal model of a two-machine parallel system is built to verify the degree of accurate distribution of reactive power theoretically.

4.1. Analysis of the Integrated Control Strategy Based on Relative Gain

The two parallel VSGs in Figure 2 are presented as examples. When the equivalent output impedance is resistive-inductive, the mutual influence between the two VSGs should be considered. At this moment, the expression of the single-phase output power of the VSG is given in (7) (the specific solution process can be found in Appendix A).

$$
\begin{align*}
    P_{e1} &= E_{12}^2 \cos \theta_{13} + E_{12}^2 \cos \theta_{12} - \frac{E_1 E_2 \cos (\delta_2 - \delta_1 - \theta_{12})}{Z_{12}} \\
    P_{e2} &= E_{23}^2 \cos \theta_{23} - E_{12}^2 \cos \theta_{12} + \frac{E_1 E_2 \cos (\delta_2 - \delta_1 - \theta_{12})}{Z_{12}} \\
    Q_{e1} &= E_{12}^2 \sin \theta_{13} + E_{12}^2 \sin \theta_{12} + \frac{E_1 E_2 \sin (\delta_2 - \delta_1 - \theta_{12})}{Z_{12}} \\
    Q_{e2} &= E_{23}^2 \sin \theta_{23} - E_{12}^2 \sin \theta_{12} - \frac{E_1 E_2 \sin (\delta_2 - \delta_1 - \theta_{12})}{Z_{12}}
\end{align*}
$$

From (7), a conclusion can be drawn that the active and reactive power output of the parallel system not only exhibits a coupling relationship between $E_i$ and $\delta_i$ but also interaction among different VSGs. Therefore, the single-machine small-signal model established in [13] cannot reflect the difference in power allocation among different DGs.
The first amplification coefficient matrix and relative gain matrix are introduced to reflect the coupling degree [26].

The matrix expression of the first amplification factor of the parallel system is given in (8).

\[
\begin{bmatrix}
\Delta P_{e1} \\
\Delta Q_{e1} \\
\Delta P_{e2} \\
\Delta Q_{e2}
\end{bmatrix}
= \begin{bmatrix}
K_{11} & K_{12} & K_{13} & K_{14} \\
K_{21} & K_{22} & K_{23} & K_{24} \\
K_{31} & K_{32} & K_{33} & K_{34} \\
K_{41} & K_{42} & K_{43} & K_{44}
\end{bmatrix}
\begin{bmatrix}
\Delta \delta_1 \\
\Delta E_1 \\
\Delta \delta_2 \\
\Delta E_2
\end{bmatrix}
\]

where \(\Delta P_{ei}, \Delta Q_{ei}, \Delta E_i,\) and \(\Delta \delta_i\) \((i = 1, 2)\) are the small disturbances of active power, reactive power, VSG output voltage, and phase angle, respectively. The specific expression of matrix element \(K\) is found in Appendix B. To illustrate the coupling situation of the two-machine parallel system intuitively and clearly, a detailed derivation of the first system’s amplification factor matrix to the relative gain matrix is presented in [26]. This derivation is used to reflect the intensity and coupling of different input-output control effects. The system parameters listed in Table 1 can be substituted into (8) to obtain the first amplification coefficient matrix expression of the system. Refer to Appendix B (A8). In addition, the expression for the relative gain matrix of the two-machine parallel system is given in (9) by using the method presented in [27].

\[
\begin{bmatrix}
\Delta \delta_1 \\
\Delta E_1 \\
\Delta \delta_2 \\
\Delta E_2
\end{bmatrix}
= \begin{bmatrix}
0.0581 & 0.9419 & 0.0584 & 0.9416 \\
0.9419 & 0.0581 & 0.9416 & 0.0584 \\
0.0584 & 0.9416 & 0.0670 & 0.9330 \\
0.9416 & 0.0584 & 0.9330 & 0.0670
\end{bmatrix}
\]

Table 1. System parameters.

| Parameter                  | Value       | Parameter                  | Value       |
|----------------------------|-------------|----------------------------|-------------|
| DC-side voltage, \(U_{dc}/\text{V}\) | 400         | Switching frequency, \(f_{\text{pwm}}/\text{kHz}\) | 5           |
| Filter inductance, \(L/\text{mH}\)   | 4           | Rated frequency, \(f_s/\text{Hz}\)       | 50          |
| Filter capacitor, \(C/\text{uF}\)    | 10          | Common load impedance, \(Z_0/\Omega\)     | 25 + j70    |
| Line impedance, \(Z_{\text{line1}}/\Omega\) | 1.5 + j0.157 | Line impedance, \(Z_{\text{line2}}/\Omega\) | 0.015 + j0.22 |
| Virtual impedance, \(Z_{v1}/\Omega\)  | −1.35 + j1.257 | Virtual impedance, \(Z_{v2}/\Omega\)     | −0.01 + j1.257 |

In accordance with (9), when the line parameters are resistive-inductive, the output power of the parallel system of the two VSGs is coupled with each other, and output power \(\Delta P_{ei}\) and \(\Delta Q_{ei}\) are considerably affected by \(\Delta E_i\) and \(\Delta \delta_i\), respectively, which do not meet the VSG control principle. The analytical formula (A8) shows that the coupling correlation between the output phase angle \(\Delta \delta_i\) and reactive power \(\Delta Q_{ei}\) is considerably greater than the influence of voltage \(\Delta E_i\) on active power \(\Delta P_{ei}\). This conclusion was proven via theoretical analysis and experiments in [28].

Virtual negative impedance control is introduced to realize the independent control of active and reactive power and reduce power coupling and the dynamic circulating current of a system. The virtual negative impedance parameters are designed according to [10]. The expression of the first amplification factor matrix is found in Appendix B (A9), and the expression of the relative gain matrix is given in (10).

\[
\begin{bmatrix}
\Delta \delta_1 \\
\Delta E_1 \\
\Delta \delta_2 \\
\Delta E_2
\end{bmatrix}
= \begin{bmatrix}
0.9968 & 0.0032 & 0.9974 & 0.0026 \\
0.0032 & 0.9968 & 0.0026 & 0.9974 \\
0.9974 & 0.0026 & 0.9970 & 0.0030 \\
0.0026 & 0.9974 & 0.0030 & 0.9970
\end{bmatrix}
\]
From (A9) and (10), a conclusion can be drawn that the coupling coefficients of \(\Delta \delta_i - \Delta P_{ei}\) and \(\Delta E_i - \Delta Q_{ei}\) are considerably larger than those of \(\Delta \delta_i - \Delta Q_{ei}\) and \(\Delta E_i - \Delta P_{ei}\), meeting the VSG control structure. The decoupling control of active and reactive power can be approximately regarded as realized. Thus, active and reactive power loops can be controlled independently.

4.2. Small-Signal Model of a Two-Machine Parallel System

To analyze the interaction among different VSGs in the system and verify the effectiveness of the integrated control strategy for accurate reactive power distribution, the following conditions are assumed to be satisfied by the system.

(1) When the virtual negative impedance control is adopted, the equivalent output impedance of the system is approximately purely inductive, realizing the decoupling of active and reactive power.

(2) The output phase angle difference of the two VSGs is extremely small and approximately regarded as \(\delta_1 - \delta_2 = 0\).

The simplified first amplification factor matrix of VSG output power, phase angle, and voltage is shown in (11).

\[
\begin{bmatrix}
\Delta P_{e1} \\
\Delta Q_{e1} \\
\Delta P_{e2} \\
\Delta Q_{e2}
\end{bmatrix} =
\begin{bmatrix}
K'_{11} & 0 & K'_{13} & 0 \\
0 & K'_{22} & 0 & K'_{24} \\
K'_{31} & 0 & K'_{33} & 0 \\
0 & K'_{42} & 0 & K'_{44}
\end{bmatrix}
\begin{bmatrix}
\Delta \delta_1 \\
\Delta E_1 \\
\Delta \delta_2 \\
\Delta E_2
\end{bmatrix}
\]

(11)

Here, the specific expression of matrix element \(K'\) is found in Appendix B (A10). By analyzing the small-signal models of the active frequency and reactive voltage control loops in (1)–(3), the theoretical expressions can be obtained as shown in (12)–(14) [29].

\[
\Delta \omega = \frac{\Delta P_{ref} - \Delta P_t}{J\omega_s + D_p\omega_s} 
\]

(12)

\[
\Delta \delta = \frac{\Delta \omega + \Delta \omega_s}{s} 
\]

(13)

\[
\Delta E = \frac{\Delta Q_{ref} - \Delta Q_e}{K_s + D_q} 
\]

(14)

When (11)–(14) are combined, the block diagram of the small-signal control of the two-machine parallel system can be obtained, as shown in Figure 5.

![Figure 5. Block diagram of the small-signal control of the two-machine parallel system.](image-url)
From Figure 5, the expressions of the reactive power output of the VSG are given in (15) and (16).

\[
\Delta Q_{e1} = (M_1(s) + N(s))\Delta Q_{ref1}
\]

\[
\Delta Q_{e2} = (M_2(s) + N(s))\Delta Q_{ref2}
\]

where \(M_i(s)\) is the transfer function formula of \(\Delta Q_{refi}\) to \(\Delta Q_{ei}\) considering the single VSG \(i\). \(N(s)\) is the transfer function formula of \(\Delta Q_{refi}\) to \(\Delta Q_{ei}\) considering the interaction of different VSGs. The specific meanings of \(M_1(s), M_2(s),\) and \(N(s)\) in the formulas are as follows:

\[
M_1(s) = \frac{2E_1Z_{12} + E_2Z_{13}}{(K_1s + D_{q1})Z_{13}Z_{12} + (2E_1Z_{12} + E_2Z_{13})}
\]

\[
M_2(s) = \frac{2E_2Z_{12} + E_1Z_{23}}{(K_1s + D_{q1})Z_{23}Z_{12} + (2E_2Z_{12} + E_1Z_{23})}
\]

\[
N(s) = \frac{-E_1E_2}{(K_1s + D_{q1})(K_2s + D_{q2})Z_{12}^2 - E_1E_2}
\]

When the traditional VSG control strategy is adopted for two parallel systems with the same capacity, the average reactive power-sharing error is shown in (17).

\[
\Delta Q_{err} = \Delta Q_{e1} - \Delta Q_{e2} = (M_1(s) - M_2(s))\Delta Q_{ref1}
\]

When the integrated control strategy is adopted, line impedance voltage drop \(\Delta U_{\text{line}}\) is added to the reactive control loop to compensate for the voltage drop on different line impedances that is equivalent to the feedback of \(U_{\text{PPC}}\). Considering the compensation of line impedance voltage drop, the matching equivalent of the impedance of different DG output lines can be realized (i.e., \(Z_{13} = Z_{23}\)). Thus, the reactive power deviation expression can be obtained, as shown in (18).

\[
\left\{ \begin{array}{l}
M_1(s) = M_2(s) \\
\Delta Q_{err} = 0
\end{array} \right.
\]

In summary, the integrated control strategy can realize the precise distribution of reactive power and power decoupling. The introduction of the local information control quantity can realize control voltage matching and the accurate droop control of user-side voltage. It can also optimize public AC bus voltage. It can meet the requirements for the “plug-and-play” control of distributed microgrids without the support of communication links.

5. Simulation and Experimental Results
5.1. Simulation Verification

To verify the feasibility and scalability of the integrated control strategy proposed in this study, a system simulation model that consists of three VSGs is established on the MATLAB/Simulink platform. The parameters of the simulation system are provided in Table 1. The line parameter design of the two latter VSGs is consistent. The control system parameters of the three VSGs are listed in Table 2. The rated capacity of the three VSGs is set as 2:1:1, and the VSGs operate parallel to the supply power to common linear loads. The differences in output power and voltage among the traditional VSG control strategy, the improved control strategy in [13], and the integrated control strategy proposed in the current study are compared. The remaining simulation conditions are identical.
Table 2. Simulation control system parameters.

| Parameter                        | VSG1 | VSG2 | VSG3 |
|----------------------------------|------|------|------|
| Virtual moment of inertia, J/(kg·m²) | 0.4  | 0.2  | 0.2  |
| Equivalent moment of inertia, K  | 15   | 15   | 15   |
| Active droop coefficient, D_p    | 5.06 | 2.53 | 2.53 |
| Reactive droop coefficient, D_q   | 350  | 175  | 175  |

The simulation operating conditions are set as follows. The common load (6.2 kW + j3.8 kVar) is initially supplied by the three VSGs operating in parallel. When \( t = 3 \) s, the load suddenly increases; that is, the common load changes to (9.1 kW + j7 kVar). When \( t = 5.5 \) s, the load suddenly increases again; that is, the common load changes to (11.3 kW + j9.9 kVar). When \( t = 8 \) s, the common load returns to the initial operating state. When \( t = 10 \) s, VSG3 exits, and VSG1 and VSG2 share the common load.

The power output waveforms of the VSG with different control strategies are presented in Figure 6. By analyzing (a), (c), and (e) in Figure 6, when the three aforementioned control strategies are adopted, active power output is consistent with achieving accurate distribution matching with its own capacity. The distribution of active power is independent of the line impedance parameters. This finding is identical to the theoretical analysis results. However, in accordance with the analysis of the reactive power output waveform in Figure 6b, the traditional VSG control strategy cannot realize the precise distribution of reactive power due to the mismatch of line parameters. The steady-state values of reactive power with different control strategies are presented in Table 3. When the line impedance parameter exhibits resistive inductance, the reactive power output will present an operating state opposite to its own capacity (e.g., 1:1.62:1.62, 1:1.3:1.3). As shown in Figure 6d and Table 3, when the control strategy proposed in [13] is adopted, the precise distribution of reactive power can be realized by combining output reactive power with virtual reactance and adjusting virtual reactance adaptively. The reactive power output between the three VSGs meets the system-rated capacity setting (i.e., 2:1:1). However, when line impedance parameters differ considerably and exhibit pure resistance, the dynamic virtual reactance parameters are too large. Reactive power cannot be accurately allocated. Furthermore, the effect of the improved control strategy in [13] highly depends on the stability of the real-time communication equipment and the accuracy of the information, and thus, robustness is poor. As shown in Figure 6f and Table 3, the application of the integrated control strategy proposed in the current study can ensure the matching of different DG control voltages in the case of mismatched line impedance parameters to complete the precise distribution requirements of reactive power. By compensating the line impedance voltage \( \Delta U_{\text{line}} \), the control of the voltage at the PCC is achieved. Compared with that in the control strategy proposed in [13], the percentage of reactive power output \( (Q_{\text{eni}}/\sum Q_{\text{eni}}) \) of the integrated control strategy as shown in Table 3 is more accurate because the reference virtual impedance is not considered. This finding is consistent with the theoretical analysis in Chapter 4. It does not need the support of communication equipment, and it meets the control requirements of “plug-and-play” for the parallel operation of different DGs. However, excessive power fluctuations will occur when VSG3 exits. The reasons for this phenomenon have yet to be discussed and analyzed.

The root mean square (RMS) of \( U_{\text{PCC}} \) with different control strategies is presented in Figure 7 and Table 4. As shown in Figure 7, the traditional VSG control cannot compensate for line impedance voltage drop, and voltage at the PCC deviates seriously from the rated value of 110 V. When load power suddenly increases, line impedance voltage drop \( \Delta U_{\text{line}} \) also increases, worsening the common bus voltage of the system. When the load power suddenly increases to (11.3 kW + j9.9 kVar), the voltage deviation of \( U_{\text{PCC}}(\Delta U_{\text{PCC}}) \) will exceed 10%. The improved control strategy proposed in [13] dynamically adjusts the output voltage of a system by combining reactive power and virtual inductance. Compared with that in the traditional VSG control strategy, the \( \Delta U_{\text{PCC}} \), as shown in Table 4, is smaller. How-
ever, this strategy does not consider the voltage drop of the benchmark virtual inductance. Moreover, it intensifies the voltage drop in the presence of a large load disturbance. The integrated control strategy proposed in the current study compensates for the line impedance voltage drop $\Delta U_{\text{line}}$ based on the VSG output terminal voltage, and it equivalently realizes control voltage forward shift, avoiding the phenomenon of $U_{\text{PCC}}$ drop caused by a change in common load power and the introduction of virtual impedance. When the load power has a large-scale, sudden increase disturbance (e.g., 11.3 kW + 9.9 kVar), the percentage of voltage sag deviation of $U_{\text{PCC}}$ with the integrated control strategy is 40% and 18.9% lower than that with the other two control strategies, respectively. It realizes precise droop control between reactive output power and common load terminal voltage $U_{\text{PCC}}$.

Figure 6. Power output waveforms of the VSG under different control strategies. (a) The traditional VSG control strategy outputs active power. (b) The traditional VSG control strategy outputs reactive power. (c) The improved control strategy outputs active power. (d) The improved control strategy outputs reactive power. (e) The integrated control strategy presented in the current study outputs active power. (f) The integrated control strategy presented in the current study outputs reactive power.
Table 3. Steady-state values of reactive power with different control strategies.

| Control Strategy           | Time                  | Qei/Var | Qei/∑Qei/N/% | Qei:Qe2:Qe3 |
|----------------------------|-----------------------|---------|--------------|-------------|
|                           | VSG1 VSG2 VSG3 VSG1 VSG2 VSG3 |         |              |             |
| Traditional VSG control   | 0 ≤ t < 3 s           | 892.6   | 1445         | 1445        | 21.2        | 38 | 38 | 1:1.62:1.62 |
|                           | 8 s ≤ t < 10 s        | 1863    | 2423         | 2423        | 26.6        | 34.6 | 34.6 | 1:1.31:1.3 |
|                           | 5.5 s ≤ t < 8 s       | 2736    | 3264         | 3264        | 27.6        | 33    | 33 | 1:1.19:1.19 |
|                           | 10 s ≤ t < 13 s       | 1521    | 2037         | 0           | 40          | 53.6 | 0 | 1:1.34 |
|                           | 0 ≤ t < 3 s           | 1843    | 921          | 921          | 48.5        | 24.2  | 24.2 | 2:1:1 |
| Improved control in [13]   | 3 s ≤ t < 5.5 s       | 3476    | 1738         | 1738        | 49.65       | 24.8  | 24.8 | 2:1:1 |
|                           | 5.5 s ≤ t < 8 s       | 4866    | 2433         | 2433        | 49.7        | 24.8  | 24.8 | 2:1:1 |
|                           | 10 s ≤ t < 13 s       | 2435    | 1218         | 0           | 64.1        | 32.1  | 0 | 2:1 |
|                           | 0 ≤ t < 3 s           | 1936    | 928          | 928          | 50.9        | 24.4  | 24.4 | 2:1:1 |
|                           | 8 s ≤ t < 10 s        | 3501    | 1750         | 1750        | 50          | 25    | 25 | 2:1:1 |
| Integrated control         | 3 s ≤ t < 5.5 s       | 4926    | 2463         | 2463        | 49.8        | 24.9  | 24.9 | 2:1:1 |
|                           | 5.5 s ≤ t < 8 s       | 2542    | 1271         | 0           | 66.9        | 33.4  | 0 | 2:1 |

Figure 7. RMS of $U_{PCC}$ with different control strategies.

Table 4. Steady-state RMS of $U_{PCC}$ with different control strategies.

| Control Strategy            | $U_{PCC}$/V | $\Delta U_{PCC}$/% | $U_{PCC}$/V | $\Delta U_{PCC}$/% | $U_{PCC}$/V | $\Delta U_{PCC}$/% | $U_{PCC}$/V | $\Delta U_{PCC}$/% |
|-----------------------------|-------------|---------------------|-------------|---------------------|-------------|---------------------|-------------|---------------------|
| Traditional VSG control    | 105.40      | -4.18               | 100.90      | -8.27               | 97.02       | -11.8               | 102.50      | -6.81               |
| Improved control in [13]    | 107.50      | -2.27               | 103.80      | -5.64               | 100.50      | -8.63               | 106.00      | -3.64               |
| Integrated control          | 108.50      | -1.36               | 105.20      | -4.36               | 102.30      | -7.00               | 107.30      | -2.45               |

5.2. Experimental Verification

To verify further the correctness of the preceding theoretical analysis and simulation results, a two-machine parallel experimental platform is built in a laboratory, as shown in Figure 8. The AINO AN51030-600 DC source is used in the DC side, Danfoss is used in the inverter circuit, and the control signal is outputted by the dSPACE real-time simulation controller. The primary circuit and control parameters of the experimental platform are consistent with those in the simulation control system.
In the first experimental condition, the capacity ratio of the two VSGs is set as 1:1 to compare the differences in power distribution, output voltage, circulation, and other aspects between the traditional VSG control and the integrated control proposed in the current study. In the second experimental condition, the capacity ratio is set as 2:1 to illustrate further the differences between the two strategies and the effectiveness of the integrated control strategy.

5.2.1. Experimental Condition 1

For the two-machine parallel system with a capacity of 1:1, the initial state of operation is a two-machine parallel operation that provides power to the common load (1.5 Kw + j600 Var). Load surge occurs after 3 s, and the common load increases (1.6 kW + j1.2 kVar). It returns to the initial operation state after 2 s. The waveforms of the experimental results using different control strategies are shown in Figure 9, where the circulating current $i_{cc}$ of the two VSGs is defined as $i_{oa1} - i_{oa2}$.

In accordance with the analysis of the VSG output active power waveforms in Figure 9a,c, the active power output of the two-machine parallel system with different control strategies is consistent. This finding is identical to the analysis of the simulation results. The VSG control strategy exerts an effect on active power. However, the traditional VSG control strategy cannot achieve reactive power-sharing, as shown in Figure 9a,c, due to the considerable difference in voltage distribution caused by the difference in line impedance. When the improved control strategy is applied, the difference caused by the impedance voltage drop of various lines can be compensated for, realizing the accurate distribution of reactive power. The specific steady-state values of reactive power are provided in Table 5. When the traditional VSG control strategy is adopted, the steady-state output reactive power deviation $\Delta Q_{err}$ is 550 Var during the initial state of the system. The reactive power deviation $\Delta Q_{err}$ is 1170 Var after the disturbance occurs. However, when the integrated control strategy proposed in the current study is applied, the output reactive power deviation $\Delta Q_{err}$ is 5 Var and 30 Var, respectively, and the reactive power-sharing effect is evident compared with that in the traditional VSG control strategy. By comparing the maximum output deviation of the instantaneous power dynamic response of the load disturbance in Figure 9a,c, a conclusion can be drawn that the control effect of the integrated control strategy is considerably better than that of the traditional VSG control strategy in suppressing reactive power dynamic deviation. The introduction of virtual negative impedance control realizes power decoupling control.
Figure 9. Waveforms of the experimental results using different control strategies in experimental condition 1. (a) The traditional VSG control strategy outputs power waveform. (b) The traditional VSG control strategy outputs the voltage effective value of $U_{PCCa}$ and circulation waveform. (c) The integrated control strategy presented in this study outputs power waveform. (d) The integrated control strategy presented in this study outputs the voltage effective value of $U_{PCCa}$ and circulation waveform.

Table 5. Steady-state values of reactive power with the same capacity.

| Control Strategy          | Reactive Power at Initial Steady-State | Reactive Power at Steady-State Perturbation |
|---------------------------|---------------------------------------|--------------------------------------------|
|                           | $Q_1$/Var | $Q_2$/Var | $Q_1$/Var | $Q_2$/Var |
| Traditional VSG control  | 30        | 580       | 250       | 1420      |
| Integrated control        | 320       | 315       | 920       | 890       |

The VSG common load terminal A-phase voltage effective value and circulating current waveform are shown in Figure 9b,d. When the traditional VSG control strategy is initially adopted, the effective value of the PCC A-phase voltage $U_{PCCa} = 107.5$ V. After the occurrence of load surge disturbance, $U_{PCCa} = 103.5$ V. When the integrated control strategy is adopted, the output side voltage $U_{PCCa} = 108.5$ V during the initial operating state and $U_{PCCa} = 107.5$ V after the disturbance. A comparative analysis shows that the integrated control strategy is equivalent to adding the voltage of $U_{PCC}$ to the reactive voltage control loop, ensuring the robustness of $U_{PCC}$ when the load is disturbed and realizing the accurate droop control of the output reactive power and user-side voltage. In accordance with the analysis of the system circulating current waveform in Figure 9b,d, the circulating current of the traditional VSG control strategy caused by the inconsistent line impedance is considerably larger than the integrated improved control strategy, and its maximum value in the dynamic switching process is more than two times that of the steady-state working current, seriously endangering the safe and stable operation of a system. Adopting the integrated control strategy can remarkably reduce the circulating current of a system. This finding is consistent with the conclusion of the simulation analysis.
5.2.2. Experimental Condition 2

The capacity of the two-machine parallel system is set to 2:1, and the operating conditions are consistent with those of the former. The waveform diagrams of the power output results using the two different control strategies are presented in Figure 10. As shown in the figure, the two control strategies can complete the output of active power capacity configuration. However, when the traditional VSG control strategy is adopted, reactive power output does not meet the configuration requirements, and the ratio of output power to capacity is the opposite. This finding is consistent with the simulation results. The specific steady-state values of reactive power are provided in Table 6. When the integrated control strategy is adopted, the reactive power of the system basically meets the set value of 2:1, verifying the effectiveness of the control strategy in parallel with different capacities.

![Waveform diagrams](image)

**Figure 10.** Waveforms of experimental results using different control strategies in experimental condition 2. (a) The traditional VSG control strategy outputs power waveform. (b) The integrated control strategy presented in this study outputs power waveform.

| Control Strategy        | Reactive Power at Initial Steady-State | Reactive Power at Steady-State Perturbation |
|-------------------------|---------------------------------------|---------------------------------------------|
|                         | $Q_1$/Var | $Q_2$/Var | $Q_1$/Var | $Q_2$/Var |
| Traditional VSG control| 430       | 210       | 1150      | 550       |
| Integrated control      | 130       | 740       | 160       | 1490      |

6. Conclusions

The precise droop control strategy of reactive power-voltage for DG parallel operation is studied in this work, and an integrated control strategy that considers line parameters is proposed. A MATLAB/Simulink model and an experimental platform are built to verify the rationality and effectiveness of the integrated control strategy. The specific conclusions are analyzed as follows.

1. The integrated control strategy can realize the precise distribution of reactive power when line impedance is not matched. The voltage of the common connection point $U_{PCC}$ is directly controlled by compensating for line impedance voltage drop. The integrated control strategy can realize precise drop control of reactive voltage, optimize public bus voltage, and improve the robustness of a system.

2. The relative gain matrix is introduced to quantify and compare the power coupling relationship before and after the improvement. The small-signal model of a two-machine parallel system is established, and the reactive power equipartition error of the integrated control strategy is derived theoretically.
(3) The proposed control strategy does not require the support of a communication system, and it can respond to load changes quickly and flexibly, providing a theoretical reference for the “plug-and-join” control of DGs.

(4) The next step is to verify the proposed improved control strategy experimentally under multiple machine operations involving three or more machines.

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**Appendix A**

When analyzing the interaction between different VSGs in the two-machine parallel system, the line impedance should be transformed through star-delta. The star equivalent circuit shown in Figure 2 is transformed into the delta equivalent circuit shown in Figure A1.

![Figure A1. Schematic diagram of conversion equivalent parallel connection.](image)

After the star-delta equivalent change, the expression of equivalent impedance is as follows:

\[
\dot{Z}_{12} = \frac{Z_1 Z_2 + Z_1 Z_0 + Z_2 Z_0}{Z_0} = Z_{12} \angle \theta_{12} \tag{A1}
\]

\[
\dot{Z}_{13} = \frac{Z_1 Z_2 + Z_1 Z_0 + Z_2 Z_0}{Z_2} = Z_{13} \angle \theta_{13} \tag{A2}
\]

\[
\dot{Z}_{23} = \frac{Z_1 Z_2 + Z_1 Z_0 + Z_2 Z_0}{Z_1} = Z_{23} \angle \theta_{23} \tag{A3}
\]
where, $Z_{12}$, $Z_{13}$, and $Z_{23}$ are the equivalent output impedance amplitudes of conversion, $\theta_{12}$, $\theta_{13}$, and $\theta_{23}$ are equivalent impedance angles. From the above equation, the output power of each branch can be expressed as follows:

$$S_1 = P_1 + jQ_1 = \frac{E_1^2}{Z_{13}} \cos \theta_{13} + j\frac{E_1^2}{Z_{13}} \sin \theta_{13}$$

$$S_2 = P_2 + jQ_2 = \frac{E_2^2}{Z_{23}} \cos \theta_{23} + j\frac{E_2^2}{Z_{23}} \sin \theta_{23}$$

$$S_3 = P_3 + jQ_3 = E_1 \angle \delta_1 \left( \frac{E_1}{Z_{12}} \angle \delta_1 \right)^*$$  \hspace{1cm} (A4)

The single-phase output power of two VSGs is expressed as:

$$P_{e1} = P_1 + P_3 = \frac{E_1^2}{Z_{13}} \cos \theta_{13} + \frac{E_2^2}{Z_{23}} \cos \theta_{23} - \frac{E_1E_2 \cos(\delta_2 - \delta_1 - \theta_{12})}{Z_{12}}$$

$$P_{e2} = P_2 - P_3 = \frac{E_2^2}{Z_{23}} \cos \theta_{23} - \frac{E_1^2}{Z_{13}} \cos \theta_{13} - \frac{E_1E_2 \cos(\delta_2 - \delta_1 - \theta_{12})}{Z_{12}}$$

$$Q_{e1} = Q_1 + Q_2 = \frac{E_1^2}{Z_{13}} \sin \theta_{13} + \frac{E_2^2}{Z_{23}} \sin \theta_{23} - \frac{E_1E_2 \sin(\delta_2 - \delta_1 - \theta_{12})}{Z_{12}}$$

$$Q_{e2} = Q_2 - Q_3 = \frac{E_2^2}{Z_{23}} \sin \theta_{23} - \frac{E_1^2}{Z_{13}} \sin \theta_{13} - \frac{E_1E_2 \sin(\delta_2 - \delta_1 - \theta_{12})}{Z_{12}}$$ \hspace{1cm} (A5)

**Appendix B**

The expression of the first amplification factor matrix $K$ of the two-machine parallel system is as follows:

$$K_{11} = \frac{-E_1E_2 \sin(\delta_2 - \delta_1 - \theta_{12})}{Z_{12}}$$

$$K_{13} = \frac{E_1E_2 \sin(\delta_2 - \delta_1 - \theta_{12})}{Z_{12}}$$

$$K_{21} = \frac{-E_1E_2 \cos(\delta_2 - \delta_1 - \theta_{12})}{Z_{12}}$$

$$K_{23} = \frac{E_1E_2 \cos(\delta_2 - \delta_1 - \theta_{12})}{Z_{12}}$$

$$K_{31} = \frac{-E_1E_2 \sin(\delta_2 - \delta_1 - \theta_{12})}{Z_{12}}$$

$$K_{33} = \frac{E_1E_2 \sin(\delta_2 - \delta_1 - \theta_{12})}{Z_{12}}$$

$$K_{41} = \frac{E_1E_2 \cos(\delta_2 - \delta_1 - \theta_{12})}{Z_{12}}$$

$$K_{43} = \frac{-E_1E_2 \cos(\delta_2 - \delta_1 - \theta_{12})}{Z_{12}}$$

\hspace{1cm} (A6)

$$\Delta P_{e1} = \begin{bmatrix} \Delta \delta_1 & \Delta E_1 & \Delta \delta_2 & \Delta E_2 \end{bmatrix} \begin{bmatrix} 3711.3 & 96.6 & -3711.3 & -96.1 \\ -14890.2 & 23.9 & 14890.2 & -23.9 \\ -3711.3 & -96.1 & 3711.3 & 96.9 \\ 14890.2 & -23.9 & -14890.2 & 27.9 \end{bmatrix}$$ \hspace{1cm} (A8)

$$\Delta Q_{e1} = \begin{bmatrix} \Delta \delta_1 & \Delta E_1 & \Delta \delta_2 & \Delta E_2 \end{bmatrix} \begin{bmatrix} 8210.8 & 3.5 & -8210.8 & -2.7 \\ -417.6 & 54.9 & 417.6 & 55.9 \\ -8210.8 & -2.7 & 8210.8 & 3.3 \\ 417.6 & -53 & -417.6 & 55 \end{bmatrix}$$ \hspace{1cm} (A9)

After introducing the virtual impedance control, the expression of the first amplification factor matrix $K'$ of the two-machine parallel system is as follows:
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\[
\begin{align*}
\Delta P_{r1} & = \Delta E_1 \frac{E_1^2 E_2}{Z_{12}} - \Delta E_2 \frac{E_1 E_2^2}{Z_{12}} \\
\Delta Q_{r1} & = \Delta E_2 \frac{E_1^2}{Z_{12}} - \Delta E_1 \frac{E_2^2}{Z_{12}} \\
\Delta P_{r2} & = -\frac{E_1 E_2}{Z_{12}} \frac{E_1}{Z_{12}} - \frac{E_1 E_2}{Z_{12}} \frac{E_2}{Z_{12}} \\
\Delta Q_{r2} & = 0
\end{align*}
\]
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