A STUDY OF RADIO POLARIZATION IN PROTOSTELLAR JETS

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ABSTRACT

Synchrotron radiation is commonly observed in connection with shocks of different velocities, ranging from relativistic shocks associated with active galactic nuclei, gamma-ray bursts, or microquasars, to weakly or non-relativistic flows such as those observed in supernova remnants. Recent observations of synchrotron emission in protostellar jets are important not only because they extend the range over which the acceleration process works, but also because they allow us to determine the jet and/or interstellar magnetic field structure, thus giving insights into the jet ejection and collimation mechanisms. In this paper, we compute for the first time polarized (synchrotron) and non-polarized (thermal X-ray) synthetic emission maps from axisymmetrical simulations of magnetized protostellar jets. We consider models with different jet velocities and variability, as well as a toroidal or helical magnetic field. Our simulations show that variable, low-density jets with velocities of ~1000 km s^{-1} and ~10 times lighter than the environment can produce internal knots with significant synchrotron emission and thermal X-rays in the shocked region of the leading bow shock moving in a dense medium. While models with a purely toroidal magnetic field show a very large degree of polarization, models with a helical magnetic field show lower values and a decrease of the degree of polarization, in agreement with observations of protostellar jets.

Key words: Herbig–Haro objects – ISM: jets and outflows – magnetohydrodynamics (MHD) – polarization – radiation mechanisms: non-thermal – shock waves

1. INTRODUCTION

Jets are present in astrophysical sources with various spatial scales, from young stellar objects (YSOs) to active galactic nuclei (AGNs). These collimated outflows are generally considered to be the result of the bipolar ejection of plasma, associated with accretion onto a central object (Blandford & Payne 1982). Variability in the ejection speed can produce internal shocks clearly seen in YSO jets in the form of bright optical knots (e.g., Raga & Noriega-Crespo 1998; Masiacardi et al. 2002) called Herbig–Haro (HH) objects.

Jets that arise from active galaxies can have relativistic speeds and are well known synchrotron radiation emitters (see for example Tregillis et al. 2001; Laing et al. 2006; Gómez et al. 2008). In contrast, YSO jets are non-relativistic and are typically thermal radio sources. However, a few stellar sources, such as Serpens (Rodriguez et al. 1989), HH 80-81 (Marti et al. 1995), Cepheus-A (Garay et al. 1996), W3(OH) (Wilner et al. 1999), and IRAS 16547-4247 (Garay et al. 2003) present radio emission with negative spectral index interpreted as non-thermal (synchrotron) radiation. Notably, polarized radio emission was detected in the jet of HH 80-81 (Carrasco-González et al. 2010). Therefore, an interesting question to answer is how jets with velocities of several hundreds km s^{-1} moving into a dense medium are able to produce shocks where particles can be accelerated up to relativistic energies and produce synchrotron radio emission.

Synchrotron maps have been computed from MHD numerical simulations by several authors in different contexts such as pulsar wind nebulae, e.g., Del Zanna et al. (2006), Volpi et al. (2008); supernova remnants, e.g., Orlando et al. (2007); and accretion disks, e.g., Goldston et al. (2005), Broderick & McKinney (2010) and Porth et al. (2011) have performed MHD numerical simulations of relativistic jets. In particular, Porth et al. (2011) have performed MHD numerical simulations of relativistic AGN jets in order to study the synchrotron emission at the jet acceleration region by computing synthetic emission maps of the spectral index, polarization degree, and rotation measure (RM). In the case of non-relativistic (YSO) jets, given the large densities of such jets at the launching region, the base of the jet is a thermal emitter. However, as the jets propagate the density decreases and non-thermal signatures can appear.

We present a polarization study in order to shed light on the understanding of the non-thermal emission in protostellar jets. We model, by using axisymmetric, magnetohydrodynamical (MHD) simulations, the synchrotron emission, and we compute the resulting polarization map. The paper is organized as follows. In Section 2, we describe the model and the numerical setup; in Section 3 we show the results (synthetic radio, polarization, and X-ray emission maps); and in Section 4 we present our conclusions.

2. NUMERICAL CALCULATIONS

2.1. Initial Setup

Our study is based on 2.5D axisymmetric, MHD simulations carried out with the adaptive mesh refinement, eulerian code {	extit{Mezcal}} (De Colle & Raga 2006; De Colle et al. 2008, 2012). We consider a 2D axisymmetrical adaptive grid, with a size of 0.2 and 0.5 pc along the r- and z-directions, respectively, and a maximum spatial resolution of $1.56 \times 10^{-2}$ pc, corresponding to 1280 × 3200 cells (at the maximum resolution) along the r- and z-directions, and six levels of refinement. The environment
in which the jet propagates is homogeneous, with a uniform density of $n_{\text{env}} = 3000 \, \text{cm}^{-3}$, a temperature of $T_{\text{env}} = 100 \, \text{K}$, and a magnetic field $B_0$. At every timestep the jet is imposed in the computational domain by rewriting the values of the physical parameters inside a region of the computational domain with $r < R_{\text{jet}} = 0.03 \, \text{pc}$ and $z < 0.003 \, \text{pc}$, with a density of $n_{\text{jet}} = 300 \, \text{cm}^{-3}$ (Araudo & Rodríguez 2012) and a velocity $v_{\text{jet}}$ (along the $z$-axis). The longitudinal magnetic field (imposed on all computational domain) is $B_z = B_0$, and the toroidal component is given by (Lind et al. 1989)

$$B_\phi(r) = \begin{cases} B_m \left( \frac{r}{R_m} \right) & 0 \leq r < R_m, \\ B_m \left( \frac{R_m}{r} \right) & R_m \leq r < R_{\text{jet}}, \\ 0 & r \geq R_{\text{jet}}, \end{cases}$$

where $R_m = 0.02 \, \text{pc}$, and $B_m$ is given in Table 1. In models M4 and M5 $B_z$ and $B_\phi$ are chosen so that $B = (\sqrt{B_z^2 + B_\phi^2})$ results of the order of 0.1 mG (Curran & Chrysostomou 2007; Carrasco-González et al. 2010). The jet pressure profile is constructed to ensure total pressure equilibrium at $t = 0$:

$$p(r) = \begin{cases} \frac{B_m^2}{8\pi} \left( \frac{r^2}{R_m^2} \beta_m - \frac{r^2}{R_m^2} \right) & 0 \leq r < R_m, \\ \frac{B_m^2}{8\pi} \left( \frac{R_m^2}{r^2} \beta_m - \frac{R_m^2}{r^2} \right) & R_m \leq r < R_{\text{jet}}, \\ \rho_{\text{env}} & r \geq R_{\text{jet}}, \end{cases}$$

where $\beta_m = \rho_{\text{env}} / (B_m^2 / 8\pi)$ and $\rho_{\text{env}} = n_{\text{env}} k_B T_{\text{env}}$.

We consider five different initial configurations. Model M1 represents a continuous jet with a constant injection velocity $v_{\text{jet}} = v_0$, whereas models M2–M5 have a time-dependent injection velocity of the form

$$v_{\text{jet}} = v_0 (1 + \Delta v \cos(\omega t)), \quad (3)$$

where $v_0 = 1000 \, \text{km} \, \text{s}^{-1}$ is the mean velocity of the flow, and $\omega = 2\pi / \tau$, $\tau = 50$ years, and $\Delta v$ is the frequency, periodicity, and amplitude of the variability, respectively. The values of $B_z$, $\Delta v$, and the jet maximum velocity $v_{\text{max}} = v_0 (1 + \Delta v)$ for the different models are given in Table 1. With these values, $v_{\text{jet}}$ is in the range of $\sim 600$–$1400 \, \text{km} \, \text{s}^{-1}$, as observed in HH 80-81 (Martí et al. 1998, 1999).

We have also explored the case of a dense and slow jet (model M6). This model has the same parameters as the model M4, except that $v_0 = 300 \, \text{km} \, \text{s}^{-1}$, $\Delta v = 0.3$, and the densities of the jet and the surrounding medium are 1000 and 100 cm$^{-3}$, respectively (see Table 1).

### Table 1

| Model | $B_z$(mG) | $B_m$(mG) | $n_{\text{env}}/n_{\text{jet}}$ | $\Delta v$ | $v_{\text{max}}$ (km s$^{-1}$) |
|-------|-----------|-----------|-------------------------------|-----------|-------------------------------|
| M1    | 0         | 0.1       | 10                            | 0         | 1000                          |
| M2    | 0         | 0.1       | 10                            | 0.2       | 1200                          |
| M3    | 0         | 0.1       | 10                            | 0.4       | 1400                          |
| M4    | 0.1/\sqrt{2} | 0.1/\sqrt{2} | 10                         | 0.4       | 1400                          |
| M5    | 0.1/\sqrt{10} | 0.3/\sqrt{10} | 10                         | 0.4       | 1400                          |
| M6    | 0.1/\sqrt{2} | 0.1/\sqrt{2} | 0.1                         | 0.3       | 390                           |

### 2.2.2. Synthetic Emission Maps

#### 2.2.2.1. Non-thermal Radio Emission and Stokes Parameters

In this section, we present a brief description of the strategy used to compute the non-thermal synchrotron emission and the Stokes parameters. For details of the method we refer the reader to Ghisellini (2013). See also Rybicki & Lightman (1986) for an in-depth description of synchrotron emission.

Synchrotron emission in YSO jets is produced by relativistic electrons accelerated in internal and termination shocks (see Section 3.1). In the present study, we assume that there is a population of relativistic electrons with a power-law energy distribution

$$n_e = K \gamma_e^{-p}, \quad (4)$$

for $\gamma_{\text{min}} \leq \gamma_e \leq \gamma_{\text{max}}$ (being $\gamma_e$ the Lorentz’s factor), and $n_e = 0$ otherwise. We fix $p = 2.1$ in our calculations and determine $K$ and $\gamma_{\text{min}}$ assuming that the number density of non-thermal electrons is a fraction $\chi_e$ ($<1$) of $n_e$, the electron density of the gas (also assuming that the plasma is composed by the same number of electrons and protons, i.e., fully ionized hydrogen, in post-shocked regions):

$$\chi_e n_e = \int_{\gamma_{\text{min}}}^{\gamma_{\text{max}}} K \gamma_e^{-p} d\gamma_e \sim K \gamma_{\text{min}}^{\gamma_{\text{max}}-p+1} / (p-1), \quad (5)$$

and that the energy density is a fraction $\chi_e$ ($<1$) of the gas kinetic energy density $\epsilon = m_e n_e \gamma_e^2 / 2$:

$$\chi_e \epsilon = \int_{\gamma_{\text{min}}}^{\gamma_{\text{max}}} K \gamma_e^{-p} (\gamma_e - 1) m_e c^2 d\gamma_e \sim K \gamma_{\text{min}}^{\gamma_{\text{max}}-p+2} / (p-2), \quad (6)$$

where $m_e$ is the rest mass of the electron and $c$ is the speed of light. From Equations (5) and (6), we obtain

$$\gamma_{\text{min}} = \frac{p-1}{p-2} \chi_e \epsilon / \chi_e n_e \gamma_{\text{min}}^{-p+1}, \quad (7)$$

and

$$K = (p-1) \chi_e n_e \gamma_{\text{min}}^{-p+1}. \quad (8)$$

We are interested in the study of the synchrotron radiation at frequencies of $\nu \sim 1 \, \text{GHz}$. This emission is optically thin at frequencies larger than the self-absorption frequency (Equation (4.56) of Ghisellini 2013)

$$\nu_{\text{sh}} = \nu_{\text{l}} \left[ \frac{\pi^{3/2} e R K \nu_{\text{sh}}^{3/2} \nu_{\text{sh}}^{(p+4)}}{4 B} \right]^{2/(p+4)}, \quad (9)$$

where $\nu_{\text{l}} = e B / (2 \pi m_e c)$ is the Larmor frequency, $e$ is the charge of the electron, and Equation (4.52) of Ghisellini 2013 is

$$f_\nu(p) \approx 3^{p+1} \left( \frac{1.8}{p^{0.7}} + \frac{p^2}{40} \right). \quad (10)$$

By setting $R = 10^{17} \, \text{cm}$ as the size of the emitting region, we obtain $\nu_{\text{sh}} \approx 3 \, \text{MHz} \ll 1 \, \text{GHz}$ for typical values of density and velocity in our simulations.

In the optically thin case, the synchrotron-specific intensity, for the isotropic case, can be written as (see Equation (4.45))
The coordinate system employed for simulating synchrotron emission. The rz-plane is the 2D plane of our axisymmetric simulation. The plane of the sky or image plane is the x'z'-plane and the y'-axis is the LOS.

Ghisellini 2013):

\[ j_\nu = \frac{3}{16} \sigma_T c K u_B \left( \frac{\nu}{\nu_L} \right)^{(1-p)/2} f_j(p), \tag{11} \]

where \( \sigma_T = 6.65 \times 10^{-25} \text{ cm}^{-2} \) is the Thomson cross-section, \( u_B = B^2/(8\pi) \) is the magnetic energy density, and \( f_j(p) \approx 3^{p/2}(2.25/p^{2.2} + 0.105) \)

(see Equation (4.46) Ghisellini 2013). Using Equations (7) and (8), Equation (11) gives

\[ j_\nu = K_i \chi_n^{1-2\alpha} \chi_e^{2\alpha} n_e n_p B_2^{\alpha+1} \nu^{-\alpha}, \tag{13} \]

where \( B_2 \) is the component of the magnetic field perpendicular to the line of sight (LOS) and \( \alpha = (p - 1)/2 = 0.55 \) is the spectral index. The factor \( K_i \) in Equation (13) is

\[ K_i = K_1 K_2 n_e^{1-3\alpha} e^{2-5\alpha} (\mu m_p)^2 \beta_2 (p), \tag{14} \]

where \( \mu \) is the molecular weight and \( m_p \) is the proton rest mass. The factors \( K_1 \) and \( K_2 \) are

\[ K_1 = (p - 1) \left( \frac{p - 2}{p - 1} \right)^{(p-1)} \tag{15} \]

and

\[ K_2 = \frac{3}{2^{2-3\alpha}} \sigma_T (\pi e)^{2\alpha-1}/2. \tag{16} \]

Synthetic synchrotron intensity maps are obtained from our 2D simulation in the following way. For each cell of our 2D axisymmetric grid we compute the synchrotron emissivity. The 2D plane of simulation (rz-plane) is tilted with respect to the plane of the sky (around the x'-axis) by an angle \( \varphi \), and it is revolved around the symmetry axis \( z \), sampling a large number of angles in the \( \theta \) direction in order to obtain a “3D distribution” of the synchrotron emissivity. Then, the emissivity \( j_\nu(\nu) \) is integrated along the LOS \( (I(\nu) = \int_{\text{LOS}} j_\nu(\nu) dy') \), which was chosen to be \( y' \) (see Figure 1). In this study, a dependence with the angle between the shock normal and the post-shocked magnetic field is not considered (see, for instance, Orlando et al. 2007; Petruk et al. 2009; and Schneiter et al. 2015 for a discussion of the acceleration mechanisms in supernova remnants).

From the synchrotron emission we have also carried a polarization study by means of maps of the Stokes parameters \( Q_B \) and \( U_B \), which can be computed as:

\[ Q_B(x', y', \nu) = \int_{\text{LOS}} f_{0} j_{\nu}(\nu) \cos[2\phi(y')] dy', \tag{17} \]

\[ U_B(x', y', \nu) = \int_{\text{LOS}} f_{0} j_{\nu}(\nu) \sin[2\phi(y')] dy', \tag{18} \]

(see, e.g., Clarke et al. 1989; Jun & Norman 1996), where \( (x', y') \) are the coordinates in the plane of the sky (see Figure 1) and \( dy' \) is measured along the LOS, \( \phi(y') \) is the position angle of the local magnetic field on the plane of the sky, and

\[ f_0 = \frac{\alpha + 1}{\alpha + 5/3}. \tag{19} \]

is the degree of linear polarization. The intensity of the linearly polarized emission is given by

\[ I_B(x', y', \nu) = \sqrt{Q_B^2(x', y', \nu) + U_B^2(x', y', \nu)} \tag{20} \]

and the map of the position angle of the magnetic field (which gives the orientation of the magnetic field in the plane of the sky) is computed as

\[ \chi_B(x', y') = \frac{1}{2} \tan^{-1}(U_B(x', y', \nu)/Q_B(x', y', \nu)). \tag{21} \]

2.2.2. Thermal X-Ray Emission

We calculated the thermal emission by integrating the free–free emissivity \( j_\nu(n_e, T) \) along the LOS. In the low-density regime, \( j_\nu(n_e, T) = n_e^2 \lambda(T) \), where \( n_e \) is the electron density and \( T \) is the temperature. As with non-thermal radio emission, we assume that the post-shocked medium is fully ionized. The function \( \lambda(T) \) was constructed with the CHIANTI atomic database (Dere et al. 1998) considering the energy range [0.15–8] keV and assuming solar metallicity.

3. RESULTS

The numerical simulations with the initial conditions summarized in Table 1 were carried out until they reach an integration time of 1500 years.

3.1. Shocks in Protostellar Jets

Figure 2 displays the number density stratification and the velocity field. As the jet interacts with the surrounding medium, it forms a double-shock structure, where the environment gas is accelerated by a forward shock, and the jet plasma is decelerated by a reverse shock. This structure, as well as the contact discontinuity separating the shocked interstellar material from the shocked jet material, is clearly visible at the head of the jet shown in Figure 2. In all cases, a slow bow shock travels against the surrounding environment with velocities \( \sim[200–260] \text{ km s}^{-1} \).

Internal shocks are present only in the models where \( \Delta v \approx 0 \). Several jumps in axial velocity are present which mark the position of the internal shocks and have values in the range [400–500] km s\(^{-1}\). With these values and the Rankine–Hugoniot jump conditions, we can estimate internal shock velocities as large as 1000 km s\(^{-1}\). These velocities, and considering that these shocks move in a low-density medium, with densities of the order of 200 cm\(^{-3}\), imply that the internal
shocks are adiabatic.\(^6\) Note that in models M3–M5 (\(\Delta v = 0.4\)) the bow shock is significantly slower (200 km s\(^{-1}\)) than in models M1 and M2 (260 km s\(^{-1}\)).

Figure 3 displays the magnitude of the magnetic field \(B\). In models M2 and M3 the jet variability is quite evident by the presence of a thin Mach disk in several internal working surfaces. In contrast, the maps corresponding to models M4 and M5 have a more complex morphology, with less defined working surfaces and a larger cocoon structure due to the magnetic field along the symmetry axis.

3.2. Radio Polarization

Figure 4 shows synthetic maps of the intensity of the linearly polarized radio emission \(I_p\), at 5 GHz, for all models. The spatial resolution of these maps is 10\(^{-3}\) pc. We have considered that the jet axis is tilted 15° with respect to the plane of the sky.

In model M1 (\(\Delta v = 0\)) the jet develops a single radio knot associated with material within the Mach disk (see Figure 4, left panel). The extended feature observed at \(z' \sim 6 \times 10^{17}\) cm,\(^5\)
associated with an internal shock, is an artifact produced by the reflective boundary condition imposed along the symmetry axis.

In contrast, the other models \((\Delta \nu = 0)\) display knotty radio structures produced by the internal shocks.\(^7\) These knots decrease in brightness with distance from the jet source. Model M4 \((B_z = B_m)\) also shows radio emission in the region behind the main bow shock. The radio emission of this region in model M5, which has \(B_z = B_m/3\) (see Table 1), results in a lower emission compared with model M4.

In Figure 5 the degree of polarization of the synchrotron radiation \((I_{\phi}(x', z', \nu)/I(x', z', \nu))\) shows an important result. Models M1–M3 exhibit a high degree of polarization of the synchrotron emission, while model M4 displays strong variations toward the symmetry axis. This behavior is also observed in model M5, although to a lesser degree. These results can be understood by considering that, in helical magnetic field, emission from regions with linearly polarized synchrotron radiation whose polarization directions are orthogonal to each other cancel out when the emission is integrated.

\(^7\) We are considering a jet with a fixed axis, and thus the working surfaces move along the axis of symmetry of the jet and never exit the cocoon carved by the main bow shock. Thus, their interaction is with the previously ejected jet material and not with the external medium.
along a LOS nearly perpendicular to the axis of symmetry of jet. A decrease of the degree of polarization has been observed in the jet associated with HH 80-81 (Carrasco-González et al. 2010).

Figure 6 displays maps of the distribution of the position angle of the magnetic field $\chi_B(x', z')$. As in observational studies, these $\chi_B(x', z')$ maps were performed from the synthetic maps of the Stokes parameters $Q_B$ and $U_B$, using Equations (17), (18), and (21). These maps show that for models M4 and M5, which display variations in the degree of polarization, the orientation of the magnetic field in the plane of the sky has a component parallel to the symmetry axis (given the additional support of the helical nature of the magnetic field), while in models M1–M3 the magnetic field is mostly perpendicular to it.

A comparison between synchrotron and thermal X-ray emission for models M3 and M4 is shown in Figure 7. For both models, the X-ray emission maps also display a knotty structure, although it is less defined than its radio counterpart. Most of the thermal X-ray emission comes from the environment material swept up by the main bow shock, as shown by Bonito et al. (2004, 2007, 2010) in hydrodynamic simulations. As it was mentioned above for the map of the linearly polarized intensity, the total synchrotron emission maps display bright knots close to the central source. These bright knots emit a radio flux, at 5 GHz, of the order of $1.5\chi_B^{1-2\alpha} \nu^{2\alpha} \times 10^{-18}$ erg s$^{-1}$ sr$^{-1}$ cm$^{-2}$ Hz$^{-1}$, which is (aside of setting the exact value for the fractions $\chi_e$ and $\chi_r$) in reasonable agreement with the flux reported by Carrasco-González et al. (2010) for the knots in HH 80-81 (1 mJy/beam or $10^{-18}$ erg s$^{-1}$ sr$^{-1}$ cm$^{-2}$ Hz$^{-1}$).

Figure 8 shows that the synchrotron emission for the case of a dense and slow jet (model M6) is 30 times lower than the emission for a lighter and faster jet (model M4). Furthermore, it is important to do a comparison of the magnitude obtained for both the non-thermal and thermal emission mechanisms in radio wavelengths. The thermal radio-continuum emission is optically thin for the parameters chosen in our simulations. Therefore, one can compute the ratio of non-thermal to thermal emissivities (using Equation (5) of Velázquez et al. (2007) and Equation (11) of this paper) in the bright radio knots of models M4 and M6 (located at $z' \simeq 1.8 \times 10^{17}$ cm and $z' \simeq 0.5 \times 10^{17}$, respectively). For model M6 this ratio is $j_\nu(\nu)/j_{\text{th}}(\nu) = 0.03$ at a frequency $\nu = 5$ GHz, while for model M4 the ratio is 1.4. Thus, a dense and slow jet does produce synchrotron emission; however, this emission is at a level that is negligible compared to the thermal radio-continuum.

4. DISCUSSION AND CONCLUSIONS

Carrasco-González et al. (2010) have shown the existence of polarized radio emission associated with the HH 80-81 protostellar jet. However, this issue has not been studied by HD or MHD simulations. We present the results obtained from 2.5D MHD simulations of low- and high-density YSO jets. We have considered cases with a constant, and a time-dependent jet ejection velocity. Furthermore, cases in which the magnetic field is toroidal or helical were analyzed.

Assuming a population of relativistic electrons that are accelerated within stellar shock jets, we have used standard prescriptions to estimate their synchrotron emission. Our results indicate that while the thermal X-ray emission is dominated by the shocked environment material at the head of the jet (in agreement with Raga et al. 2002; Bonito et al. 2004, 2007, 2010), the non-thermal radio emission turns out to be dominated by the jet material inside the internal shocks.

Also, radio maps reveal that the variability in jet velocity is important for generating bright knots of synchrotron emission, produced when slow jet material is caught up by faster jet material.

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8 The opacity $\tau_\nu$ is $\ll 1$, considering Equation (3) of Velázquez et al. (2007).
Our models show that a jet with a toroidal magnetic field emits synchrotron radiation with a high degree of polarization. In contrast, models with a helical magnetic field exhibit a decrease on the degree of polarization, in good agreement with observational results (Carrasco-González et al. 2010).

Finally, our results indicate that non-negligible synchrotron emission can be obtained in low-density and high-velocity protostellar jets.

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Figure 7. Comparison of synthetic synchrotron emission maps at $\nu = 5$ GHz (left panels) with thermal X-ray emission maps (right panels) for models M3 and M4 (top and bottom panels, respectively). The synchrotron emission is given in units of $x_{\nu}^{1-2x_{\nu}}$ [erg cm$^{-2}$ s$^{-1}$ sr$^{-1}$ Hz$^{-1}$], while the thermal X-ray emission is in units of erg cm$^{-2}$ s$^{-1}$ sr$^{-1}$.

Figure 8. Comparison of synthetic synchrotron emission maps, at 5 GHz, of model M4 (left panel) with model M6 (right panel). The synchrotron emission is given in units of $x_{\nu}^{1-2x_{\nu}}$ [erg cm$^{-2}$ s$^{-1}$ sr$^{-1}$ Hz$^{-1}$].

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