Satellitesimal Formation via Collisional Dust Growth in Steady Circumplanetary Disks

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Abstract

The icy satellites around Jupiter are considered to have formed in a circumplanetary disk. While previous models have focused on the formation of the satellites starting from satellitesimals, the question of how satellitesimals themselves form from smaller dust particles has not yet been addressed. In this work, we study the possibility that satellitesimals form in situ in a circumplanetary disk. We calculate the radial distribution of the surface density and representative size of icy dust particles that grow by colliding with each other and drift toward the central planet in a steady circumplanetary disk with a continuous supply of gas and dust from the parent protoplanetary disk. The radial drift barrier is overcome if the ratio of the dust-to-gas accretion rates onto the circumplanetary disk, $\dot{M}_d/\dot{M}_g$, is high and the strength of turbulence, $\alpha$, is not too low. The collision velocity is lower than the critical velocity of fragmentation when $\alpha$ is low. Taken together, we find that the conditions for satellitesimal formation via dust coagulation are given by $\dot{M}_d/\dot{M}_g \geq 1$ and $10^{-4} \leq \alpha < 10^{-2}$. The former condition is generally difficult to achieve, suggesting that the in situ satellitesimal formation via particle sticking is viable only under extreme conditions. We also show that neither satellitesimal formation via the collisional growth of porous aggregates nor via streaming instability is viable as long as $\dot{M}_d/\dot{M}_g$ is low.

Key words: accretion, accretion disks – planets and satellites: formation – turbulence

1. Introduction

The gas giants in the solar system have large satellites whose orbits are on the same plane. These regular satellites are believed to have formed in gas disks around the planets, called circumplanetary disks, like protoplanetary disks that form planets around stars (Lunine & Stevenson 1982). Numerical simulations show that circumplanetary disks are by-products of gas accretion from the parent protoplanetary disk to the gas giants (e.g., Lubow et al. 1999; D’Angelo et al. 2002; Tanigawa et al. 2012; Fung & Chiang 2016; Szulágyi et al. 2016).

Satellite formation in circumplanetary disks has been studied extensively. Lunine & Stevenson (1982) proposed the minimum-mass disk model where the circumplanetary disk is static and its solid mass is equal to the total mass of the satellites. Mosqueira & Estrada (2003a, 2003b), Estrada (2009), and Mosqueira et al. (2010) showed that the Jovian and Saturnian satellites can form in the minimum-mass disks with a low-density outer portion, although the satellites would have to overcome rapid inward migration induced by the interaction with the massive disk (Miguel & Ida 2016). Canup & Ward (2002) and Ward & Canup (2010) proposed the gas-starved disk whose mass is regulated by viscous accretion onto the central planet and by a gradual supply of the gas from the parent protoplanetary disk. They showed that the temperature of the disk is sustained low enough to produce icy satellites. Alibert et al. (2005) also developed a similar accretion disk model that is consistent with a formation model for Jupiter. Canup & Ward (2006) performed N-body simulations of satellite formation in the gas-starved disk, showing that the total mass of the satellites formed in the disk is $\sim 10^{-4}$ of the central planet’s mass, as observed for the Jovian, Saturnian, and Uranian satellite systems. Sasaki et al. (2010) and Ogihara & Ida (2012) also studied the satellite formation in the gas-starved disk model using Monte Carlo and N-body simulations, respectively, and successfully reproduced the number, masses, and orbits of the Galilean satellites. Sasaki et al. (2010) also reproduced the Saturnian system.

One significant problem for these satellite formation studies is that how satellitesimals form from dust particles are unaddressed. Canup & Ward (2006), Sasaki et al. (2010), and Ogihara & Ida (2012) assumed that the dust particles grow to satellitesimals as soon as they are delivered from the protoplanetary to the circumplanetary disks. However, it is already known from planetesimal formation studies that dust growth to kilometer-sized bodies in protoplanetary disks can be hindered by phenomena such as the radial drift and the collisional fragmentation of intermediate-sized particles (Whipple 1972; Adachi et al. 1976; Weidenschilling 1977). Therefore, it is easy to imagine that satellitesimal formation in circumplanetary disks could suffer from similar difficulties.

In this work, we aim to answer the question of whether dust particles can grow to satellitesimals by their direct collisional growth in circumplanetary disks. We employ a simple one-dimensional model in which we calculate the radial distribution of the surface density and typical size of dust particles in a steadily accreting circumplanetary disk. We also consider only icy dust particles and do not consider rocky particles. Although we assume perfect sticking upon collision, fragmentation occurs if the collision velocity is higher than a few m s$^{-1}$ when the aggregates are mainly composed of silicate particles (e.g., Blum & Wurm 2008; Wada et al. 2009). The majority of the Galilean satellites are indeed icy satellites: Europa is $\sim$10% and Ganymede and Callisto are $\sim$50% ice by mass (Sohl et al. 2002). Our simple treatment allows us to explore a large parameter space. The goal of this work is to derive the conditions under which satellitesimal formation via direct coagulation of dust particles is viable.

We note that it has also been discussed that planetesimals can be captured by gas drag from the circumplanetary disks (Fujita et al. 2013; Tanigawa et al. 2014; D’Angelo &...
Podolak 2015; Suetsugu et al. 2016; Suetsugu & Ohtsuki 2017). Suetsugu et al. (2016) and Suetsugu & Ohtsuki (2017) examined the captures and subsequent orbital evolutions of planetesimals. They showed that the capture hypothesis could roughly reproduce the initial radial distribution of planetesimals (i.e., planetesimals) assumed in the satellite formation model by Canup & Ward (2006), Sasaki et al. (2010), and Ogihara & Ida (2012). However, if there is a gas gap around the circumplanetary disk, the positive pressure gradient outside of the gap removes low eccentricity planetesimals from the feeding zone of the planet and the capture rate decreases (Kobayashi et al. 2012; Fujii et al. 2013; Tanigawa et al. 2014; Suetsugu & Ohtsuki 2017).

The structure of this paper is as follows. In Section 2, we describe our model for the circumplanetary gas disk and explain how we treat the collisional growth and radial drift of the dust particles in the disk. In Section 3, we show the results of our calculations and derive the conditions for successful planetesimal formation via dust coagulation. In Section 4, we discuss the feasibility of the conditions and consider other probabilities of planetesimal formation. Finally, we conclude this paper in Section 5.

2. Methods

2.1. Circumplanetary Disk Model

We model the structure of the circumplanetary disk following Fujii et al. (2014). Although some numerical simulations suggested the possibility that gas near the midplane spirals outward (Tanigawa et al. 2012; Fung & Chiang 2016; Szulágyi et al. 2016), here we assume that the circumplanetary disk is a viscous accretion disk with a continuous supply of material from the protoplanetary disk. The diffusion equation for the gas surface density \( \Sigma_g \) of the circumplanetary disk is then given by

\[
\frac{\partial \Sigma_g}{\partial t} = \frac{1}{r} \frac{\partial}{\partial r} \left[ 3r^{1/2} \frac{\partial}{\partial r} \left( r^{1/2} \nu \Sigma_g \right) \right] + f,
\]

where \( r \) is the distance from the central planet, \( f \) is the mass flux of the gas inflow from the protoplanetary to the circumplanetary disks, and \( \nu \) is the kinematic viscosity. We employ the standard \( \alpha \) prescription (Shakura & Sunyaev 1973) and express the viscosity as \( \nu = \alpha c_s H_g \), where \( c_s \) is the isothermal sound speed and \( H_g \) is the gas scale height. The sound speed is related to the temperature as \( c_s^2 = \frac{k_b T}{m_g} \), with \( k_b \) as the Boltzmann constant and \( m_g \) as the mean molecular mass. The gas scale height is given by \( H_g = c_s / \Omega_K \), where \( \Omega_K = \sqrt{GM_p / r^3} \) is the Kepler frequency, and \( G \) and \( M_p \) are the gravitational constant and the central planet mass, respectively. Unless otherwise noted, we assume \( M_p \) to be the Jupiter mass, \( M_p = 1.89 \times 10^{30} \) g. Based on the results of the three-dimensional hydrodynamical simulation by Tanigawa et al. (2012), Fujii et al. (2014) modeled \( f \) as \( f \propto r^{-1} \) for \( r < r_b \) and \( f = 0 \) for \( r > r_b \), where \( r_b \) is the radius of the region where the gas falls in. With this scaling for \( f \), the steady-state solution of Equation (1) can be analytically obtained as (see Equations (23) and 25 of Fujii et al. 2014)

\[
\Sigma_g = \frac{M_g}{2 \pi r_b} \frac{r^{3/2}}{\nu} \left( -\frac{2}{9} r^{-1/2} + \frac{2}{3} r_b r^{-3/2} \right).
\]

where \( M_g \) is the mass accretion rate of the infall gas. The simulation by Tanigawa et al. (2012) shows that \( r_b \approx 20 R_J \) for the planet of \( M_p = 0.4 M_J \) (see also Fujii et al. 2014). Assuming that \( r_b \) scales with the Hill radius of the central planet, we use \( r_b = 27 R_J \) for our 1M\( J \)-mass planet.

We assume that the circumplanetary disk is viscously heated. Then, the gas temperature at the midplane is given by Nakamoto & Nakagawa (1994),

\[
T = \left( \frac{9}{8 \sigma_{SB}} \nu \Sigma_g \Omega_K \right)^{1/4} g(\tau),
\]

where \( \sigma_{SB} \) is the Stefan–Boltzmann constant and

\[
g(\tau) = \left( \frac{3}{8} \tau + \frac{1}{4.8 \tau} \right)^{1/4}
\]

is a function of the Rosseland mean optical depth \( \tau \). In principle, \( \tau \) depends on the size distribution of the smallest dust particles, which cannot be predicted with simple dust evolution models as employed in this study. Lacking good knowledge of \( \tau \), we opt to set \( g \approx 1 \). Since \( g \approx 1 \) in general, the assumption \( g \approx 1 \) yields a minimum estimate for the disk temperature. The temperature can be up to three times higher than what is assumed here if the optical depth ranges between \( 10^{-2} \lesssim \tau \lesssim 10^2 \). However, this uncertainty has little effect on the main results of this work because the dependence of our results on \( T \) is weak (see Section 3.2).

According to the simulation by Tanigawa et al. (2012), the mass flux \( M_g \) scales as \( M_g \approx 0.2 \Sigma_{PPD} \Omega_{H} \Omega_{PPD} \), where \( \Sigma_{PPD} \) and \( \Omega_{PPD} \) are the gas surface density and orbital period of the parent protoplanetary disk in the vicinity of the planet, respectively, and \( n_H \) is the planet’s Hill radius (see Figure 14 of Tanigawa et al. 2012). At Jupiter’s orbit, the gas surface density is 143 g cm\(^{-2}\) according to the minimum-mass solar nebula model of Hayashi (1981). For this value of \( \Sigma_{PPD} \), the accretion rate onto a Jupiter-sized planet would be \( M_g \approx 200 M_J \) Myr\(^{-1}\).

However, a strong constraint on \( M_g \) can be obtained from the temperature of the circumplanetary disk. In the left panel of Figure 1, we plot the midplane temperature of our modeled circumplanetary disk as a function of the distance from the central planets for three cases \( M_g = 2, 0.2, 0, 0.02 \) and 0.002 \( M_J \) Myr\(^{-1}\). For \( M_g = 2 \) and 0.2 \( M_J \) Myr\(^{-1}\), the temperatures are higher than the sublimation temperature of ice, which is about 160 K. Such hot environments are unsuitable for the formation of icy regular satellites around Jupiter and Saturn. Therefore, we only consider \( M_g \leq 0.02 M_J \) Myr\(^{-1}\) in this work. We plot the gas surface density of the disk for the two cases in the right panel of Figure 1.

2.2. Dust Growth and Radial Drift

We treat the coagulation and radial drift of dust particles in circumplanetary disks. In particular, we focus on the steady-state where the radial distribution of the size and surface density of the particles is constant over time. We approximate the size distribution of the particles at each distance from the central planet by a narrow distribution peaked at mass \( m_d \). With
the collisional cross section of the gas
is the relative velocity between the dust particles

\( \dot{M}_g = \frac{4R_d \Delta \nu \delta_\text{gas}}{\nu \lambda_{\text{mfp}}} \)

where \( \Delta \nu \) is the relative velocity between the dust particles and the gas, and \( C_D \) is a dimensionless coefficient that depends on the particle Reynolds number, \( \text{Re}_p \). According to Perets & Murray-Clay (2011), the coefficient can be written as

\[
C_D = \frac{24}{\text{Re}_p} \left( 1 + 0.27 \text{Re}_p^{0.47} \right) \times \left( 1 - \exp(-0.04 \text{Re}_p^{0.38}) \right).
\]

The particle Reynolds number is given by

\[
\text{Re}_p = \frac{4R_d \Delta \nu \delta_\text{gas}}{\nu_{\text{th}} \lambda_{\text{mfp}}},
\]

where \( \nu_{\text{th}} = \sqrt{8/\pi \sigma_{\text{visc}}} \) is the thermal velocity and \( \lambda_{\text{mfp}} = m_g/(\sigma_{\text{mol}} \rho_g) \) is the mean free pass of the gas with \( \sigma_{\text{mol}} = 2 \times 10^{-15} \text{ cm}^2 \) the collisional cross section of the gas molecules and \( \rho_g = \Sigma_g/(\sqrt{2\pi} H_g) \) is the gas density at the midplane.

The scale height of the particles can be derived analytically from the balance of their vertical sedimentation and diffusion (Youdin & Lithwick 2007),

\[
H_g = H_g \left( 1 + \frac{\text{St} \left( 1 + 2\text{St} \right)}{\alpha \left( 1 + \text{St} \right)} \right)^{-1/2}.
\]

The radial drift velocity of the dust particles is (Whipple 1972; Adachi et al. 1976; Weidenschilling 1977)

\[
v_r = -2 \frac{\text{St}}{\text{St}^2 + 1} \eta \nu_k.
\]
where \( \nu_k = r \Omega_k \) is the Kepler velocity and

\[
\eta = -\frac{1}{2} \left( \frac{H_g}{r} \right)^2 \frac{\partial \ln \rho_g c_s^2}{\partial \ln r} \tag{12}
\]

is the ratio of the pressure gradient force to the gravity of the central planet.

The relative velocity between the dust particles (i.e., collision velocity) is the root square

\[
\Delta \nu_{dld} = \sqrt{\Delta \nu_B^2 + \Delta \nu_p^2 + \Delta \nu_c^2 + \Delta \nu_s^2 + \Delta \nu_t^2}, \tag{13}
\]

where \( \Delta \nu_B, \Delta \nu_p, \Delta \nu_c, \Delta \nu_s, \) and \( \Delta \nu_t \) are the relative velocities induced by Brownian motion, the radial drift, azimuthal drift, vertical sedimentation, and turbulence (Okuzumi et al. 2012). For collisions between equal-sized particles, the Brownian-motion-induced velocity can be written as

\[
\Delta \nu_B = 16k_B T/(\pi m_d). \tag{16}
\]

The relative velocity induced by the radial drift is \( \Delta \nu_p = \nu_p(S_0) - \nu_p(S_2) \), where \( S_1 \) and \( S_2 \) are the Stokes numbers of the two particles. We assume \( S_2 = 0.5S_1 \) (see Section 2.4 in Sato et al. 2016) and \( \nu_p \) is given by Equation (11). The relative velocity induced by the azimuthal drift is \( \Delta \nu_c = \nu_c(S_0) - \nu_c(S_2) \), where \( \nu_c = -\nu_k/(1 + S_t^2) \). The relative velocity induced by the vertical motion is \( \Delta \nu_s = \nu_s(S_0) - \nu_s(S_2) \), where \( \nu_s = -\Omega_k S_t H_d/(1 + S_t) \). For the relative velocity induced by the turbulence, we use the analytic formula derived from Ormel & Cuzzi (2007). The formula has three limiting expressions:

\[
\Delta \nu_t = \begin{cases} 
\sqrt{\alpha c_s \text{Re}_t^{1/4}} |S_0 - S_2|, & S_t \ll \text{Re}_t^{-1/2}, \\
\sqrt{3\alpha c_s \text{Re}_t^{1/2}}, & \text{Re}_t^{-1/2} \ll S_t \ll 1, \\
\sqrt{\alpha c_s \left( \frac{1}{1 + S_t} + \frac{1}{1 + S_2} \right)}^{1/2}, & 1 \ll S_t.
\end{cases} \tag{14}
\]

Here, \( \text{Re}_t = \nu / \nu_{\text{mol}} \) is the turbulence Reynolds number, where \( \nu_{\text{mol}} = \nu_k \lambda_{\text{Dust}} / 2 \) is the molecular viscosity. We obtain the relative velocity between the solid materials and the gas, \( \Delta \nu_{\text{gld}} \), by setting \( S_0 = S_t \) and \( S_2 \rightarrow 0 \) in the above expressions for the relative velocities.

2.3. Parameter Choice

Table 1 summarizes the parameter range explored in this study. The gas infall rate \( \dot{M}_g \) onto the circumplanetary disk is taken to be either 0.02 \( M_J \) Myr\(^{-1}\) or 0.002 \( M_J \) Myr\(^{-1}\). As mentioned in Section 2.1, we do not consider a higher value of \( \dot{M}_g \) since the disk would become too hot for icy satellites to form. In reality, a giant planet carves a gap around its orbit. For example, the hydrodynamical simulations by Kanagawa et al. (2015) show that the gas surface density inside the gap is depleted by a factor of more than 100 compared to that outside the gap. This means that realistic values of \( \dot{M}_g \) should be less than 2 \( M_J \) Myr\(^{-1}\), i.e., less than 1% of the accretion rate without a gap. The infall rate that was adopted in the gas-starved disk model of Canup & Ward (2002) is about 0.2 \( M_J \) Myr\(^{-1}\). The value of \( \dot{M}_g \), whose temperature is suitable for icy satellite formation is lower than these estimated values. Although we do not consider the decrease of the gas inflow in detail, the final phase of planetary formation should be suitable for satellite formation (see also Section 4.1).

The ratio \( \dot{M}_g / \dot{M}_b \) of the dust infall rate to the gas inflow rate is chosen between 0.001–1. If we assume that the inflow has a solar composition and the dust particles are strongly coupled with the gas, the ratio should be 0.01. However, the gap structure of the gas around Jupiter dams the dust particles that drifted from the outer region of the protoplanetary disk toward the Sun, and generates their similar gap structure. On the other hand, the strong gas gradient may trigger a hydrodynamic instability and disturb the gas inflow. This disturbance should enhance the radial diffusion of small dust particles and make them nearer to the central planet (Zhu et al. 2012; Tanigawa et al. 2014).

The strength \( \alpha \) of turbulence is varied from \( 10^{-5} \) to \( 10^{-2} \). We note that the mechanisms that could drive turbulence in the circumplanetary disk are highly uncertain. The magnetorotational instability, a viable mechanism driving turbulence in ionized accretion disks, could operate on the surface of circumplanetary disks (Turner et al. 2014), but might not produce fully developed turbulence (Fujii et al. 2014). Therefore, we cannot rule out that \( \alpha \) of circumplanetary disks falls below \( \alpha \). However, as we discuss in the following section, turbulence that is too weak could make it difficult for satellites to form within a realistic range of \( \dot{M}_g / \dot{M}_b \).

3. Results

In this section, we present the results of our dust growth calculations and explore the conditions under which satellites could form through dust coagulation in circumplanetary disks.

3.1. Fiducial Calculations

Figure 2 shows the results of our fiducial calculations that assume \( \dot{M}_g = 0.02 M_J \) Myr\(^{-1}\) and \( \alpha = 10^{-4} \). We assume that the snowline is where the midplane temperature is 160 K and it is at \( r = 10 R_\text{J} \) (see Figure 1). The top, middle, and low panels represent the surface density, radius, and Stokes number of the mass-dominating dust particles in the disk as a function of the distance \( r \) from the central planet. Because the particles grow and move inward at the same time, the particle size increases with decreasing \( r \). As already mentioned in the previous section, we assume that the dust particles are 0.1 mm in size when they are initially delivered from the protoplanetary disk to \( r = r_{\text{p}} (=27R_\text{J}) \). However, the middle panel of Figure 2 suggests that the assumption about the initial size of the dust particles is not crucial because the particles immediately grow whenever they reach the snowline.
Figure 2. Steady-state profiles of the surface density $\Sigma_d$ (top panel) and radius $R_d$ (middle panel) of dust particles that grow and drift in the circumplanetary disk of $M_\bullet = 0.02 M_\odot$ Myr$^{-1}$ and $\alpha = 10^{-4}$. The bottom panel shows the Stokes number $St$ of the particles. The red, green, blue, and purple curves correspond to $M_d/M_\bullet = 1, 0.1, 0.01$, and 0.001, respectively. The dashed lines in the bottom panel show the prediction from the analytic estimate given by Equation (15). Shaded gray is the region interior to the snowline, which lies at $r = 10 R_\oplus$.

their drift timescale $t_{\text{drift}} = r/v_d$ becomes shorter than 30 times the growth timescale $t_{\text{grow}} = m_d/(dm_d/dr)$, in agreement with the situation for dust evolution in protoplanetary disks (Okuzumi et al. 2012; Tsukamoto et al. 2017). For $M_d/M_\bullet = 1$, we find that the particles stop drifting and grow to kilometer-sized satellitesimals at $r \sim 10 R_\oplus$. The drift stalls because the drift speed (normalized by $v_{\text{kip}}$) decreases with increasing size as long as $St > 1$. Therefore, they have to overcome this barrier of the $St = 1$ for growing to become satellitesimals. After they achieve $St = 1$, the drift speed becomes slower and they become jammed. The jam makes the collisional rate higher, so the collisional growth speeds up. We also found that this condition $St > 1$ is consistent with $t_{\text{grow}} < t_{\text{drift}}$ when $St \sim 1$. Note that we did not consider the possibility that the dust surface density near the snowline increases because of sublimation or recondensation (e.g., Saito & Sirono 2011; Ros & Johansen 2013; Ida & Guillot 2016; Ida et al. 2016; Schoonenberg & Ormel 2017).

### 3.2. Effects of the Dust and Gas Inflow Mass Fluxes

The amount of gas and dust that flows to the circumplanetary disk can be changed by the conditions of the central planet, the protoplanetary disk, and the circumplanetary disk. We investigate the effects of changing the gas and dust inflow mass fluxes. Figure 2 shows that the the dust surface density increases with the dust-to-gas inflow mass flux ratio $M_d/M_\bullet$. The radius and Stokes number of the dust particles also have the same features. The particles can grow to satellitesimals only when $M_d/M_\bullet = 1$. This can be understood by using the approximate analytical expression for the Stokes number (dotted lines in the figure). When $\alpha = 10^{-4}$ and $M_\bullet = 0.02 M_\odot$ Myr$^{-1}$, the gas surface density is so large that $Re_p \ll 1$. For example, we found that the particle Reynolds number $Re_p$ is about $10^3$ when $M_d/M_\bullet = 0.1 - 1$ at $r \sim 10 R_\oplus$. In this case, the dimensionless coefficient $C_D$ can be approximated as a constant, $C_D \approx 0.5$ (Newton’s friction law, see Equation (8)). The dust–dust and dust–gas relative velocities can also be approximated as $\Delta v_{\text{rel}} \approx (1/2) v_{\text{in}}$ and $\Delta v_{\text{rel}} \approx v_{\text{in}}$ because the turbulence is so week that $\Delta v_{\text{rel}}$ is much smaller than $v_{\text{in}}$. The approximated Stokes number can then be described as

$$St \approx 1.2 \left( \frac{M_d/M_\bullet}{1} \right)^{2/5} \left( \frac{\alpha}{10^{-4}} \right)^{1/5} \left( \frac{T}{160 \, \text{K}} \right)^{-2/5} \left( \frac{M_{\text{cp}}}{1 M_\odot} \right)^{2/5} \left( \frac{r}{10 R_\oplus} \right)^{-2/5},$$

(15)

for small $r$. Equation (15) is derived by substituting Equation (6) into Equation (5) and integrating it. Here, the gas surface density and the midplane temperature have been approximated as $\Sigma_g \approx M_\bullet \Omega_K / (3 \pi \alpha c_s^2)$ and $T \approx (3 G M_{\text{cp}} M_\bullet / (8 \pi \Sigma_g R_\oplus^3))^{1/4}$. The scale height and radial drift velocity of the dust particles have also been approximated as $H_d \approx H_g (\alpha/Sp)^{1/2}$ and $\Delta v_d \approx 2St v_{\text{kip}}/K$. Equation (15) shows that the Stokes number is proportional to $(M_d/M_\bullet)^{2/5}$ and reaches unity when $M_d/M_\bullet = 1$ and $r = 10 R_\oplus$. Once $St$ exceeds unity, the radial drift velocity starts to decrease with increasing particle size, and hence the particles grow to satellitesimals. Ignoring the weak $M_\bullet$ dependence of $T \propto M_\bullet^{1/4}$, $\Sigma_g$ is proportional to $M_\bullet$. When $\Sigma_g$ is high, the gas drag force that the dust particles receives is strong and $St$ is small. The collision rate of the dust particles becomes high when $M_d$ (i.e., $\Sigma_d$) is large. The high collision rate promotes satellitesimal formation. Even if the Newton’s friction law does not apply, the Stokes number is proportional to $(M_d/M_\bullet)^{2/3}$ or $(M_d/M_\bullet)^{6/11}$ and the trend that the Stokes number is an increasing function does not change (see Equations (16) and (17) in the Appendix).
The key parameter of the dust evolution is not the pure gas in\textsuperscript{low mass flux but the ratio of the dust and gas in\textsuperscript{low mass fluxes. Figure 3 represents the distribution of the dust surface density, dust radius, and Stokes number of the representative dust particles for \( \dot{M}_g = 0.002 \dot{M}_j \text{ Myr}^{-1} \) and \( \alpha = 10^{-4} \). In this case, the snowline lies at \( r = 5R_j \) (see Figure 1). The profiles of the surface density and radius of dust particles are lower than those for \( \dot{M}_g = 0.02 \dot{M}_j \text{ Myr}^{-1} \) and \( \alpha = 10^{-4} \) (Figure 2). The radial profiles of St are steeper than those in the fiducial case (we derive Equation (16), an analytic equation of St for \( \dot{M}_g = 0.002 \dot{M}_j \text{ Myr}^{-1} \), in the Appendix). Nevertheless, we find that dust particles grow beyond St = 1 only when \( \dot{M}_d / \dot{M}_g = 1 \). For fixed \( \dot{M}_d / \dot{M}_g \), the \( \dot{M}_g \) dependence of St is indeed weak. When \( \dot{M}_g = 0.02 \dot{M}_j \text{ Myr}^{-1} \), only T depends on \( \dot{M}_g \) (\( T \propto \dot{M}_g^{1/5} \)), so St \( \propto T^{-2/5} \propto \dot{M}_g^{-1/10} \) (Equation (15)). When \( \dot{M}_g = 0.002 \dot{M}_j \text{ Myr}^{-1} \) or \( \alpha = 10^{-2} \), St \( \propto T^{-1} \propto \dot{M}_g^{4/9} \propto \dot{M}_g^{7/36} \) or St \( \propto T^{-1} \propto \dot{M}_g^{4/11} \propto \dot{M}_g^{5/44} \) (Equations (16) and (17)).

3.3. Effects of the Strength of Turbulence

The strength of turbulence in the circumplanetary disk is also a key parameter of the dust evolution. Figure 4 represents the profiles of the dust particles in the case with \( \dot{M}_g = 0.02 \dot{M}_j \text{ Myr}^{-1} \) and \( \alpha = 10^{-5} \) (upper panel) and \( \alpha = 10^{-2} \) (lower panel). The dashed lines in the upper and lower panels show the predictions from the analytic estimates given by Equations (15) and (17), respectively.
high enough for the particles to overcome the radial drift outside the snowline unless $M_d/M_g \geq 1$.

Even if $M_d/M_g = 1$, satellitesimals would not form via direct dust growth because the relative velocity between the dust particles would be too high to avoid collisional fragmentation. Collision simulations by Wada et al. (2009) argued that icy dust aggregates with monomers of 0.1 $\mu$m fragment upon collision if the collision velocity is higher than 50 m s$^{-1}$. Figure 5 represents the dust–dust relative velocities for different values of $\alpha$. When $\alpha = 10^{-4}$, the relative velocity is determined by the radial drift speed and that induced by the turbulence is low. When $\alpha = 10^{-2}$, the dust–dust relative velocity is determined by the turbulence because the relative velocity induced by the turbulence is proportional to $\sqrt{\alpha}$ (Equation (14)) and it becomes 10 times higher than that for $\alpha = 10^{-4}$. Figure 5 shows that the relative velocity exceeds 50 m s$^{-1}$, indicating that collisional fragmentation would happen. Therefore, satellitesimal formation via direct dust coagulation is unlikely to occur in such strong turbulence. Note that experiments by Gundlach & Blum (2015) showed that the fragmentation occurs with a collision speed of $\sim$10 m s$^{-1}$ for icy aggregates with monomers of 1 $\mu$m.

3.4. Conditions for Satellitesimal Formation

The results presented in the previous subsections can be summarized in Figure 6. This figure represents the condition for satellitesimal formation when $M_g = 0.02 M_J$ Myr$^{-1}$. The conditions are $M_d/M_g \geq 1$ and $10^{-4} \leq \alpha < 10^{-2}$. The condition for breaking through the radial drift barrier is approximately given by $M_d/M_g > 6 \times 10^{-3} \times \alpha^{-1/2}$ derived from the condition $St > 1$ at $r = 10 R_J$ (see Equation (15)). When the turbulence is strong ($\alpha \gtrsim 10^{-3}$), it is about $M_d/M_g > 0.08 \alpha^{-1/6}$ (see Equation (17)). The dashed lines in Figure 6 show the boundary of each condition. However, in the case of $\alpha = 10^{-2}$, the aggregate collision velocity is too high to avoid collisional fragmentation. When $M_g = 0.002 M_J$ Myr$^{-1}$, the drift barrier is overcome outside the snowline even if $\alpha = 10^{-5}$ because the line is at $r = 5 R_J$ (asterisk in Figure 6).

Figure 5. Dust–dust relative velocities with different turbulence strengths, $\alpha = 10^{-4}$ (left panel) and $\alpha = 10^{-2}$ (right panel). The other conditions are $M_d/M_g = 1$ and $M_g = 0.02 M_J$ Myr$^{-1}$ in both panels. The black curves represent the dust–dust relative velocities (collision velocities). The red and blue curves represent the velocities induced by only the turbulence and their radial drift, respectively. The black dashed lines are the critical velocity of fragmentation.

Figure 6. Condition for satellitesimal formation when $M_g = 0.02 M_J$ Myr$^{-1}$. The green ticks indicate that dust particles grow to satellitesimals outside of the snowline at $r = 10 R_J$. The red crosses indicate that the radial drift barrier inhibits dust growth to satellitesimals. The blue triangles indicate that dust particles grow to satellitesimals in the calculations, but the collision velocity (dust–dust relative velocity) is faster than the critical velocity of fragmentation, 50 m s$^{-1}$. The dashed lines show the condition $St = 1$ at $r = 10 R_J$ from Equations (15) and (17). When $M_g = 0.002 M_J$ Myr$^{-1}$, the condition is the same except that the drift barrier is overcome outside the snowline if $M_d/M_g = 1$ and $\alpha = 10^{-5}$ (asterisk).

4. Discussions

4.1. Feasibility of the High Dust-to-gas Inflow Mass Flux Ratio

We found that the one of the conditions for satellitesimal formation is $M_d/M_g \geq 1$. However, this condition may be difficult to achieve. First, since the dust particles tend to settle down toward the midplane, the inflow gas from the high altitude is likely to be dust-poor gas (Tanigawa et al. 2012). This effect must depend on the conditions of the turbulence and the gas density of the region around the circumplanetary disk that the accretion gas comes from (Equations (15) and (10)). Second, the dust supply may not be enough to achieve $M_d/M_g \geq 1$. Dust particles are drifted from the outer region of the protoplanetary disk. However, these particles have already grown to the size of pebbles (centimeter-sized particles) until
they reach around gas planets like Jupiter (e.g., Lambrechts & Johansen 2012; Okuzumi et al. 2012; Sato et al. 2016), so most of them should be damped at the outer edge of the gas gap by the positive gas pressure gradient (e.g., Adachi et al. 1976; Zhu et al. 2012). In this case, only a small part of the dust particles can penetrate into the gas gap and flow into the circumplanetary disk, so the dust-to-gas mass inflow flux ratio should be smaller than unity.

One possibility for achieving the high ratio is by considering satellitesimal formation in the final phase of planetary formation. Photoevaporation may increase the dust-to-gas mass ratio in protoplanetary disks as time passes (e.g., Alexander et al. 2006a, 2006b). It is also considered that the gas flux decreases in the final phase because the gas gap becomes wider and deeper (e.g., Kanagawa et al. 2015; Tanigawa & Tanaka 2016). Our results actually suggested that a low gas inflow mass flux is suitable for satellitesimal formation. The midplane temperature $T$ is almost proportional to $M_g^{1.4}$ (Equation (3)). When the gas inflow decreases, the disk becomes cooler and the snowline moves inward (see Figure 1). This means that the area where icy satellitesimals can form expands. Moreover, the collisional velocity driven by turbulence weakly depends on the gas inflow rate, $\Delta v_\text{coll} \propto c_s \propto T^{1/2} \propto M_g^{7/8}$ (Equation (14)). A low gas inflow mass flux may also contribute to overcoming the fragmentation barrier.

4.2. Effects of the Internal Density

We investigated the impact of changing the internal density of dust particles on satellitesimal formation. Figure 7 represents the Stokes number for $\rho_{\text{int}} = 1.4 \times 10^{-4} \, \text{g cm}^{-3}$ and $\alpha = 10^{-4}$. We found that the conditions for satellitesimal formation did not change from those with $\rho_{\text{int}} = 1.4 \, \text{g cm}^{-3}$ (see Figures 2 and 3). This is because the Stokes number for small $r$ can also be approximated as Equation (15) in this case, (we found that $\text{Re}_p \gtrsim 10^8$ for $r \sim 10 \, R_\text{g}$ and we have been able to assume $C_D \approx 0.5$) and this approximated Stokes number dose not depend on $\rho_{\text{int}}$. Generally, the growth timescale takes a minimum value within the Newton regime (Okuzumi et al. 2012). Therefore, the Stokes number does not grow beyond the dashed lines in Figure 7 by changing $\rho_{\text{int}}$ unless it reaches unity. The impact of changing $\rho_{\text{int}}$ is only that the fluffy particles move earlier than the compact particles from the Stokes regime ($\text{Re}_p \lesssim 1$) to the Newton regime.

4.3. Streaming Instability

Generating growing particle-density perturbations by streaming instability is another planetsimal formation mechanism not applicable to the collisional growth of the dust particles (Youdin & Goodman 2005). The difference between the velocities of the dust and gas drives the instability. The dust particles are concentrated quickly in localized dense clumps, so they do not drift to the Sun. This mechanism may also be applicable to satellitesimal formation. Carrera et al. (2015) showed that the condition that streaming instability is active depends on the dust-to-gas surface density ratio and the Stokes number of the dust particles. They found that the particle clumps can form if $\Sigma_d/\Sigma_g > 0.02$ in the most suitable Stokes number condition (see Figure 8 in Carrera et al. 2015). However, our results showed that the ratio is much lower than the critical value (see Figure 8), so it should be difficult to form satellitesimals via the streaming instability process. Note that water sublimation or recondensation near the snowline can result in an enhancement in the dust surface density and may be able to trigger streaming instability (Ida & Guillot 2016; Ida et al. 2016; Schoonenberg & Ormel 2017).

4.4. Validity of the Single-size Approach in Circumplanetary Disks

We used a single-size approach to investigate the growth and drift of dust particles in circumplanetary disks. As shown by Sato et al. (2016), this approach is valid for the growth and drift of mass-dominating particles in protoplanetary disks, as long as the collisional destruction of the particles is negligible (see also Krijt et al. 2016, Okuzumi et al. 2016, and Tsukamoto et al. 2017 for applications to dust growth in protoplanetary disks).

In principle, the single-size approximation breaks down when there is more than one population of particles that dominates the total dust mass. Unlike our assumption that the dust inflow onto the circumplanetary disk is concentrated at the outer edge of the
gas inflow region, the dust inflow may be extended over a wide area of the disk. In this case, the size distribution in the inner disk regions may have two peaks, one for the drifting pebbles that accreted in the outer disk region and one for the small dust grains directly supplied to the inner disk regions. Actually, when the dust particles strongly couple with the gas, the mass flux of the dust inflow should be proportional to that of the gas $f \propto r^{-1}$. The ratio of the dust mass flux flowing to the inside of $r$ relative to the total dust inflow mass flux is then $\approx r/r_\text{p}$, which is still about 0.5 even if $r = 15 R_J$ (the orbit of Ganymede). Therefore, the actual size distribution of the dust particles may be wide. We note that our assumption of a concentrated dust inflow may have also caused overestimation of the Stokes number, especially in the outer disk regions ($\text{St} \propto M_g^{2/5}, M_g^{1/3},$ or $M_g^{6/11}$ in our model; see Equations (15)–(17)) and the satellitesimal formation could be harder in reality.

On the other hand, even if the dust particles have a wide size distribution, the smaller particles should grow rapidly and the distribution will narrow. This is because the dust growth timescale $t_{\text{grow}}$ must be an increasing function of the dust mass $m_d$ in the Newton regime ($t_{\text{grow}} \propto m_d^{1/3}$ or $m_d^{2/3}$ in our model; see Equations (5)–(7), and the approximations in Section 3.2 and the Appendix), so the dust particles should grow as orderly growth in most areas within the disk. However, the $m_d$ dependence of $t_{\text{grow}}$ is weak and in the future we will have to make sure of the validity of the single-size approach by using full-size calculations of dust growth in circumplanetary disks.

5. Conclusions

We have investigated whether icy dust particles can form satellitesimals by their pairwise collisional growth in circumplanetary disks with various conditions. We have calculated the distribution of the surface density, radius, and Stokes number of the peak mass dust particles. Our model considered only steady conditions and assumed that the temperature of the circumplanetary disk is almost like a minimum estimate. The gas inflow and the circumplanetary disk model were based on the results of Tanigawa et al. (2012) and Fuji et al. (2014). We have changed the dust and gas inflow mass fluxes and the strength of turbulence in the disk so that we understood the effects of these factors on satellitesimal formation. We have also approximated the Stokes number (normalized stopping time) of dust particles to understand these effects because satellitesimals can form only when the Stokes number achieves unity. From these parameter studies, we have revealed the conditions for satellitesimal formation and discussed their feasibility. We have also discussed the effects of changing the internal density of dust particles and the possibility of satellitesimal formation by streaming instability. Our findings are summarized as follows.

1. The mass flux of dust and gas flowing into the circumplanetary disk determines the evolution of dust particles. Particularly, the dust-to-gas inflow mass flux ratio, $M_d/M_g$, is important. A larger dust inflow provides a higher dust density in the circumplanetary disk, accelerating collisional dust growth. A small amount of gas inflow makes the gas surface density of the circumplanetary disk lower and the gas drag force that dust particles receive weaker. This reduces the radial drift speed of the particles and this is advantageous for collisional growth. The approximated Stokes number is actually proportional to $(M_d/M_g)^{7/5}$, $(M_d/M_g)^{2/3}$, or $(M_d/M_g)^{6/11}$ (Equations (15)–(17)). As a result, satellitesimals can form only for $M_d/M_g \gtrsim 1$. For fixed $M_d/M_g$, the Stokes number depends on the gas inflow mass flux only: $M_g^{1/10}, M_g^{7/36}$, or $M_g^{6/44}$ (Equations (15)–(17)), so the key parameter is not the pure gas (or pure dust) inflow mass flux but the ratio of the dust and gas mass inflow.

2. The strength of turbulence also affects the fate of dust particles. When $M_d = 0.02 M_J$ Myr$^{-1}$, the approximated Stokes number is proportional to $\alpha^{1/5}$ or $\alpha^{1/11}$ (Equations (15) and (17)). As a result, satellitesimals can form only for $\alpha \gtrsim 10^{-4}$. Moreover, strong turbulence increases the collisional velocity and it actually exceeds the critical fragmentation velocity of 50 m s$^{-1}$ (Wada et al. 2009) when $\alpha = 10^{-2}$ (Figure 5).

In summary, the conditions for satellitesimal formation via collisional dust growth are $M_d/M_g \gtrsim 1$ and $10^{-4} \lesssim \alpha < 10^{-2}$ when $M_g = 0.02 M_J$ Myr$^{-1}$ (Figure 6). This result does not strongly depend on the gas inflow mass flux.

Our results also suggest that the porosity of dust particles does not affect the condition for satellitesimal formation (Section 4.2). The Stokes number of dust particles takes the largest value in the Newton regime and the value does not depend on the internal density (Equation (15)). Low internal density just makes the particles go into the Newton regime quickly.

In reality, it would be difficult to achieve the condition $M_d/M_g \gtrsim 1$ (Section 4.1). In protoplanetary disks, the majority of dust in the vicinity of gas giants should settle down to the midplane so that the inflow gas from the high altitude may be dust-poor. The dust particles also have already grown to pebble-sized particles. Such large particles may not accrete onto circumplanetary disks, because they are easily trapped at the edges of planet-carved gas gaps (Zhu et al. 2012).

Satellitesimal formation via streaming instability is also unfeasible (Section 4.3). The dust-to-gas surface density ratio $\Sigma_d/\Sigma_g$ is much smaller than the critical value 0.02 where the instability occurs.

However, the photoevaporation may contribute to satisfying the condition for satellitesimal formation by increasing the dust-to-gas ratio of the inflow gas (Section 4.1). The final phase of planetary formation should also be suitable for satellitesimal formation because of the wide and deep gas gap. The smaller the gas inflow mass flux becomes, the lower temperature and the slower collision velocity become.
The delivery of planetesimals from the protoplanetary disk may be necessary for satellite formation around gas giants. As we mentioned in Section 1, the planetesimal capture hypothesis can roughly reproduce the initial radial distribution of planetesimals assumed in the previous satellite formation models (Suetsugu & Ohtsuki 2017). Moreover, the captured planetesimals may efficiently accrete the drifting dust particles that could not grow to planetesimals in the circumplanetary disk. Such a satellite formation scenario via pebble accretion will be investigated in our future work.

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Appendix

Approximation of the Stokes Number for Low-gas-density Cases

This assumption is not correct when the gas density is low via small gas inflow mass flux or strong turbulence. When $\dot{M}_g = 0.002 M_J \text{ Myr}^{-1}$ and $\alpha = 10^{-4}$, or $\dot{M}_g = 0.002 M_J \text{ Myr}^{-1}$ and $\alpha = 10^{-2}$, the particle Reynolds number is within the range of $10^{-1} \lesssim \Re_P \lesssim 10^2$ for $r \sim 10 R_J$. In this case, $C_D$ can be approximated as $C_D \approx 12/\sqrt{\Re_P}$ (Equation (8)). When $\dot{M}_g = 0.002 M_J \text{ Myr}^{-1}$ and $\alpha = 10^{-4}$, the dust–dust and dust–gas relative velocities are approximated as $\Delta v_{\text{rel}} \approx (1/2) v_t$ and $\Delta v_{\text{rel}} \approx v_t$. The Stokes number $St$ can then be approximated as

$$\text{St} \approx 1.6 \left( \frac{\dot{M}_d/\dot{M}_g}{1} \right)^{2/3} \left( \frac{\alpha}{10^{-2}} \right)^{-1/9} \left( \frac{\dot{M}_g}{0.002 M_J \text{ Myr}^{-1}} \right)^{4/9} \times \left( \frac{T}{90 \text{ K}} \right)^{-1} \left( \frac{\rho_{\text{int}}}{1.4 \text{ g cm}^{-3}} \right)^{-2/9} \left( \frac{M_{\text{up}}}{1 M_J} \right)^{7/9} \left( \frac{r}{10 R_J} \right)^{-13/9},$$

(16)

for small $r$. Unlike in Equations (15) and (17), $St$ decreases with increasing $\alpha$, although the dependence is very weak. Strong turbulence disperses dust particles into the vertical direction and thereby reduces their collision rate (see Equations (5) and (10)). However, this effect is canceled out by the particle collision velocity induced by turbulence, which increases with increasing $\alpha$. When $\dot{M}_g = 0.02 M_J \text{ Myr}^{-1}$ and $\alpha = 10^{-2}$, the two relative velocities are determined by the strength of turbulence (i.e., $\Delta v_{\text{rel}} \approx \Delta v_{\text{rel}} \approx \sqrt{3 \alpha} c_s S t^{1/2}$, see Figure 5),

$$\text{St} \approx 0.73 \left( \frac{\dot{M}_d/\dot{M}_g}{0.1} \right)^{6/11} \left( \frac{\alpha}{10^{-2}} \right)^{1/11} \left( \frac{\dot{M}_g}{0.02 M_J \text{ Myr}^{-1}} \right)^{4/11} \times \left( \frac{T}{160 \text{ K}} \right)^{-1} \left( \frac{\rho_{\text{int}}}{1.4 \text{ g cm}^{-3}} \right)^{-2/11} \left( \frac{M_{\text{up}}}{1 M_J} \right)^{9/11} \left( \frac{r}{10 R_J} \right)^{-15/11},$$

(17)

for small $r$.