1. INTRODUCTION

Natural heat transfer has gained importance in the last three decades for its various applications, such as cooling electronic devices and reducing energy leakage from energy conservation storages [1–4]. Aydin et al. [5] used the stream function-vorticity formulation to study the effect of aspect ratio within rectangular enclosures. They found that the effects of Rayleigh number and aspect ratio on heat transfer were more significant and stronger, respectively, when the enclosure was shallow. Specifically, when the enclosure was tall, the Rayleigh number was high. Basak et al. [6, 7] used a square cavity to study the influence of distributed heating on natural convection. They showed that thermal mixing and heat distribution inside a square cavity were highly enhanced compared to those in the isothermal hot bottom wall. Moreover, the overall heat transfer was lower for the nonuniform heating case compared to that for the uniform heating case. The unsteady laminar natural convection flow for saturated porous was illustrated by Hossain and Wilson [8] using a rectangular enclosure. The non-isothermal left wall, hot bottom wall, cold top, and right walls were used in their work. Results showed that the porosity of the medium increased for the walls with decreasing volumetric flow rate and heat transfer rate of fluid. Song and Viskanta [9] theoretically and experimentally explained the natural convection flow inside a rectangular enclosure partly filled with an anisotropic porous medium. Volume-averaged conservation equations were used to consider the effect of the anisotropic flow characteristics of the porous medium on flow and heat transfer. Natural convection flows in a square cavity filled with a porous matrix was studied by Sathiyananth et al. [10]. The local Nusselt number exhibited an oscillatory nature due to the presence of multiple secondary circulations. The average Nusselt numbers were almost constant through an entire range of Rayleigh up to $10^6$ for $Da = 10^{-5}$, Darcy number ($10^4$ ≥ $Da ≥ 10^3$), nanoparticle volume fraction $(0 ≤ φ ≤ 0.1)$, and porous layer thickness $(0 ≤ γ ≤ 100\%)$.

Keywords: natural convection, nanofluid, trapezoidal enclosure, porous media, finite element technique.
independent of the cavity orientation at a low value of Rayleigh number. Lyican et al. [14] attempted to study heat transfer by natural convective flow in a trapezoidal enclosure with parallel cylindrical top and bottom walls at different temperatures and adiabatic side walls. Hyun and Choi [15] used the finite difference method to numerically study transient natural convective heat transfer in a parallelogram-shaped enclosure with high Rayleigh numbers. With a parallelogram-shaped enclosure utilized as a transient thermal diode, they identified the importance of tilt angle by using it to control the partition walls of the enclosure. Varol et al. [16] studied natural convection within trapezoidal enclosures partially cooled from the inclined wall and the heat transfer and fluid flow caused by buoyancy forces in divided trapezoidal enclosures. The divider had constant thermal conductivity. Results showed that the conduction mode of heat transfer prevailed within the cavity for low Rayleigh numbers, low thermal conductivity ratio, and high partition thickness.

The effect of nanoparticles on convection heat transfer and fluid flow has been mentioned in several research, such as Alsabery et al. [17], who numerically studied the problem of Darcian natural convection in a trapezoidal cavity partly filled with porous layer and partly with nanofluid layer. Results showed that the addition of Ag–water nanofluid clearly increased the convection, and the inclination angle of the cavity variation had an important effect on heat transfer rate. The effect of nanoparticles on natural convection and entropy generation in a semicircular enclosure filled with nanofluid (Cu water) was presented in Al-Zamily and Amin [18]. Results showed that the heat transfer rate increased with an increase in Rayleigh number and nanoparticle volume fraction. System irreversibility increased as nanoparticle volume fraction increased. Al-Zamily and Amin [19] studied the fluid flow, heat transfer, and entropy generation within a square cavity embedded with heat flux and subject to the horizontal magnetic field. Results revealed that the effect of the Hartmann on Nusselt number increased as the Darcy number increased, especially at high Rayleigh numbers. Moreover, at Ra = 10^7 and Φ = 0.15, the percentage decreased in the Nusselt number owing to the presence of a magnetic field (Ha = 40). The values were 85.89% at Da = 10^{-1}, 87.12% at Da = 10^{-3}, and 98.69% at Da = 10^{-5}. Finally, finite element technique (FET) was used to numerically study natural convection heat transfer within a trapezoidal enclosure filled with Ag nanofluid and saturated porous medium with the same nanofluid.

2. MATHEMATICAL MODEL

The dimensionless Navier–Stokes and energy equations for nanofluid and porous–nanofluid medium within a trapezoidal enclosure was solved numerically using FET. The fluid flow was considered laminar, incompressible, 2-D, and steady without internal heat generation. The thermophysical properties of the nanofluid were assumed to be constant, except for density in the Y-direction of the momentum equation. Local thermal equilibrium along with the Darcy–Brinkman model was used to model the saturated porous medium. Figure 1 illustrates a diagram of the trapezoidal enclosure with an inner adiabatic circular cylinder within. The cavity was subdivided into two layers; the top was filled with Ag nanofluid and the bottom with a saturated porous medium mixed with the same nanofluid. The central bottom length (L_h = 0.5) was considered to maintain isotherm hot temperature while the other length of the bottom wall was kept adiabatic. The two-inclined lines with an angle and the circular cylinder were kept adiabatic.

2.1 Governing dimensional equations

The equations for the nanofluid represented are as follows [20, 21]:

\[
\begin{align*}
\frac{\partial u_{na}}{\partial x} + \frac{\partial v_{na}}{\partial y} &= 0 \\
\rho_{na}(u_{na}\frac{\partial u_{na}}{\partial x} + v_{na}\frac{\partial u_{na}}{\partial y}) &= -\frac{\partial p}{\partial x} + \mu_{na}\left(\frac{\partial^2 u_{na}}{\partial x^2} + \frac{\partial^2 u_{na}}{\partial y^2}\right) \tag{2}
\end{align*}
\]

\[
\begin{align*}
\rho_{na}(u_{na}\frac{\partial v_{na}}{\partial x} + v_{na}\frac{\partial v_{na}}{\partial y}) &= -\frac{\partial p}{\partial y} + \mu_{na}\left(\frac{\partial^2 v_{na}}{\partial x^2} + \frac{\partial^2 v_{na}}{\partial y^2}\right) \tag{3}
\end{align*}
\]

\[
\begin{align*}
\rho_{na}\frac{\partial T_{na}}{\partial x} + v_{na}\frac{\partial T_{na}}{\partial y} &= \alpha_{na}\left(\frac{\partial^2 T_{na}}{\partial x^2} + \frac{\partial^2 T_{na}}{\partial y^2}\right) \tag{4}
\end{align*}
\]

The governing equations for the porous media partition [19] are as follows:

\[
\begin{align*}
\frac{\partial u_{po}}{\partial x} + \frac{\partial v_{po}}{\partial y} &= 0 \tag{5}
\end{align*}
\]
\[ X - \text{momentum} \]
\[ \rho_{na} \left( u_{po} \frac{\partial u_{po}}{\partial x} + v_{po} \frac{\partial u_{po}}{\partial y} \right) = -\epsilon^2 \frac{\partial \rho}{\partial x} + \epsilon \mu_{na} \left( \frac{\partial^2 u_{po}}{\partial x^2} + \frac{\partial^2 u_{po}}{\partial y^2} \right) \]
\[ Y - \text{momentum} \]
\[ \rho_{na} \left( u_{po} \frac{\partial v_{po}}{\partial x} + v_{po} \frac{\partial v_{po}}{\partial y} \right) = -\epsilon^2 \frac{\partial \rho}{\partial y} + \epsilon \mu_{na} \left( \frac{\partial^2 v_{po}}{\partial x^2} + \frac{\partial^2 v_{po}}{\partial y^2} \right) \]

Energy
\[ u_{po} \frac{\partial T_{po}}{\partial x} + v_{po} \frac{\partial T_{po}}{\partial y} = \alpha_{eff} \left( \frac{\partial^2 T_{po}}{\partial x^2} + \frac{\partial^2 T_{po}}{\partial y^2} \right) \]

where \( \rho \) is the density, \( \alpha \) is the thermal diffusivity, \( \mu \) is the dynamic viscosity, \( \epsilon \) is the porosity, \( K \) is the permeability, \( \beta \) is the thermal expansion coefficient, and \( na, po, \) and \( fl \) are the subscripts for nanofluid, porous medium, and pure fluid, respectively.

Suppose the relation for stream function \( \psi \)
\[ \left( v = -\frac{\partial \psi}{\partial x} \right) \], and vorticity \( \left( \omega = \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right) \) are presented in the dimensionless parameters as follows:

\[ X = \frac{x}{L}, Y = \frac{y}{L}; U = \frac{uL}{\alpha_{fl}}, V = \frac{vL}{\alpha_{fl}}, P = \frac{pL^2}{\rho_{na} \alpha_{fl}^2} \]
\[ Da = \frac{k_{fl}}{L^2}, \theta = \frac{T - T_c}{T_h - T_c} \]
\[ Ra = \frac{g \beta_{fl}(T_h - T_c) L^3}{\nu_{fl} \alpha_{fl}}; Pr = \frac{\nu_{fl}}{\alpha_{fl}} = \frac{\nu}{\alpha_{fl}} = \frac{\nu}{\alpha_{fl}} \]

The physical properties of the nanofluid can be expressed as follows [22]:
\[ \rho_{na} = (1 - \varphi) \rho_{fl} + \varphi \rho_{po} \]
\[ (\rho \beta)_{na} = (1 - \varphi) (\rho \beta)_{fl} + \varphi (\rho \beta)_{po} \]
\[ \alpha_{na} = \frac{K_{na}}{(\rho \rho_{p})_{na}} \]
\[ \alpha_{eff} = \frac{K_{eff}}{(\rho \rho_{p})_{na}} \]
\[ K_{eff} = (1 - \epsilon) K_s + \epsilon K_{na} \]

\[ (\rho \epsilon_{p})_{na} = (1 - \varphi) \left( (\rho \epsilon_{p})_{fl} + \varphi (\rho \epsilon_{p})_{po} \right) \]
\[ K_{na} = K_{fl} \left( \frac{K_{po} + 2K_{fl}}{K_{po} + 2K_{fl} + \varphi K_{fl} - K_{po}} \right) \]
\[ \mu_{na} = \mu_{fl} (1 - \varphi)^{2.5} \]

The dimensionless equations take the following forms:

Continuity
\[ \frac{\partial U_{na}}{\partial X} + \frac{\partial V_{na}}{\partial Y} = 0 \]

X - momentum
\[ U_{na} \frac{\partial U_{na}}{\partial X} + V_{na} \frac{\partial U_{na}}{\partial Y} = -\frac{\partial P}{\partial X} + \frac{Pr \rho_{fl}}{\rho_{na}} \left( \frac{\partial^2 U_{na}}{\partial X^2} + \frac{\partial^2 U_{na}}{\partial Y^2} \right) \]

Y - momentum
\[ U_{na} \frac{\partial V_{na}}{\partial X} + V_{na} \frac{\partial V_{na}}{\partial Y} = -\frac{\partial P}{\partial Y} + \frac{Pr \rho_{fl}}{\rho_{na}} \left( \frac{\partial^2 V_{na}}{\partial X^2} + \frac{\partial^2 V_{na}}{\partial Y^2} \right) + \frac{(\rho \beta)_{na}}{\rho_{na} \beta_{fl}} Ra Pr \theta_{na} \]

Energy
\[ U_{na} \frac{\partial T_{na}}{\partial X} + V_{na} \frac{\partial T_{na}}{\partial Y} = \frac{\partial^2 T_{na}}{\partial X^2} + \frac{\partial^2 T_{na}}{\partial Y^2} \]

The dimensionless form of the governing equations for the porous media domain will be written as:

Continuity
\[ \frac{\partial U_{po}}{\partial X} + \frac{\partial V_{po}}{\partial Y} = 0 \]

X - momentum
\[ U_{po} \frac{\partial U_{po}}{\partial X} + V_{po} \frac{\partial U_{po}}{\partial Y} = -\frac{\partial P}{\partial X} + \frac{Pr \rho_{fl}}{\rho_{na}} \left( \frac{\partial^2 U_{po}}{\partial X^2} + \frac{\partial^2 U_{po}}{\partial Y^2} \right) \]
\[ -\frac{Pr \rho_{fl}}{\rho_{na}} U_{po} \]

Y - momentum
\[ U_{po} \frac{\partial V_{po}}{\partial X} + V_{po} \frac{\partial V_{po}}{\partial Y} = -\frac{\partial P}{\partial Y} + \frac{Pr \rho_{fl}}{\rho_{na}} \left( \frac{\partial^2 V_{po}}{\partial X^2} + \frac{\partial^2 V_{po}}{\partial Y^2} \right) \]
\[ -\frac{Pr \rho_{fl}}{\rho_{na}} V_{po} \]
\[ U_{po} \frac{\partial \theta_{po}}{\partial X} + V_{po} \frac{\partial \theta_{po}}{\partial Y} = \alpha_{na} \left( \frac{\partial^2 \theta_{po}}{\partial X^2} + \frac{\partial^2 \theta_{po}}{\partial Y^2} \right) \] \tag{24}

The boundary conditions on the outside walls of the enclosure are shown in Table 1.

### Table 1. Boundary conditions for the enclosure

| Position             | Direction | U, V, Ψ | 0         |
|----------------------|-----------|---------|-----------|
| Left side wall       | Y = H     | 0, 0, 0 | \( \frac{\partial \theta}{\partial n} = 0 \) |
| Right side wall      | Y = H     | 0, 0, 0 | \( \frac{\partial \theta}{\partial n} = 0 \) |
| Bottom wall          | X = L-L_b | 0, 0, 0 | \( \frac{\partial \theta}{\partial Y} = 0 \) |
| Bottom wall          | X = L_b   | 0, 0, 0 | 1         |
| Top wall             | X = L_c   | 0, 0, 0 | 0         |

The thermo-physical properties of the Ag nanofluid are shown in Table 2.

### Table 2. Properties of pure water and Cu nanoparticles as presented in Ref. [23]

| Properties | \( C_p \) (J/kg·k) | \( \rho \) (kg/m³) | \( k \) (W/m·k) | \( B \) (1/k) | \( \mu \) (kg/m·s) |
|------------|---------------------|-------------------|----------------|-------------|-----------------|
| Ag         | 235                 | 10500             | 429            | 1.89×10^{-5} | -               |
| Pure water | 4179                | 997.1             | 0.613          | 21×10^{-5}  | 0.000372        |

The conditions applied to the permeable surfaces between the porous partition and nanofluid can be defined as:

\[
\begin{align*}
\theta_{po} &= \theta_{na}, \quad \frac{\partial \theta_{na}}{\partial X} = \frac{K_{eff} \cdot \partial \theta_{po}}{K_{na} \cdot \partial X}, \\
\Psi_{po} &= \Psi_{na}, \quad \frac{\partial \Psi_{na}}{\partial X} = \frac{\partial \Psi_{po}}{\partial X}, \\
\Omega_{po} &= \Omega_{na}, \quad \frac{\partial \Omega_{na}}{\partial X} = \frac{\partial \Omega_{po}}{\partial X}, \\
\mu_{po} \left( \frac{\partial U_{po}}{\partial Y} + \frac{\partial V_{po}}{\partial X} \right) &= \mu_{na} \left( \frac{\partial U_{na}}{\partial Y} + \frac{\partial V_{na}}{\partial X} \right), \\
P_{po} &= P_{na}, \quad \frac{\partial P_{po}}{\partial X} = \frac{\partial P_{na}}{\partial Y}
\end{align*}
\] \tag{25}

The local and average Nusselt numbers for the hot wall are determined as follows:

\[
\begin{align*}
N_{lu_{local}} &= \frac{K_{na}}{K_{fl}} \frac{1}{\pi} \frac{\partial \theta}{\partial n} \quad \tag{26} \\
N_{lu_{ave}} &= \frac{K_{na}}{K_{fl}} \frac{1}{0} \frac{\partial \theta}{\partial n} \quad \tag{27}
\end{align*}

### 2.2 Validation

To ensure the accuracy of the present work, the numerical results were validated with those of Kim et al. in terms of streamlines and isotherms for the inner cylinder located inside a square enclosure filled with air as a working fluid (Figure 2).

The numerical grid generation is presented in Figure 3, which also illustrates a triangular fine mesh for the trapezoidal enclosure.

### 3. RESULTS AND DISCUSSION

#### 3.1 Influence of Rayleigh number

This section discusses the influence of Rayleigh number on streamlines and isotherms for saturated porous medium–Ag nanofluid (lower layer) with the same nanofluid (upper layer) at \( (Da = 0.001, \varphi = 0.1, \gamma_P = 0.5) \). Figure 4a shows that when the Rayleigh number increased from \( Ra = 10^4 \) to \( Ra = 10^6 \), the maximum absolute value of stream function increased from \( |\Psi_{max}| = 0.015405 \) to \( |\Psi_{max}| = 3.6520 \), respectively. The physical reason is due to the improving fluid flow strength and intensity as the Rayleigh number increased. The convection heat transfer is dominated at high Rayleigh number values, which lead to increased stream function.

For the isotherm contours, Figure 4b shows that when the Rayleigh number is low, the isotherms have horizontal uniform shapes due to the dominated...
conduction heat transfer and the weak influence of convection fluid flow. However, when the Rayleigh number is low (Ra = 10^6), a clear change in isotherm contours can be noted. The isotherm shapes change their behavior from the horizontal pattern into the curved pattern. In this case, the convective heat transfer mode is dominated.

When the Darcy number increases from Da = 10^{-5} to Da = 0.01, the maximum absolute value of the isothermal lines becomes denser around the heat source and reaches a maximum value at hot wall 0.95 and minimum value at cold wall 0.045. This outcome is attributed to the increase in fluid flow activity as the Darcy number increases. In this case, the thickness of the boundary layer caused by aggregation of isothermal lines around the heat source decreases; thus, the heat transfer rate is enhanced.

### 3.3 Influence of porous layer thickness

Figure 6 displays the influence of vertical changes in the porous layer thickness on fluid flow strength and isotherm contours at Ra = 10^6, Da = 0.001, and ϕ = 0.1. When the porous layer thickness increases from Y_p = 0.2 to Y_p = 0.8, the maximum absolute value of stream function decreases from |ψ_{max}| = 4.6054 to |ψ_{max}| = 2.66 due to the resistance of the porous layer hydrodynamic.
minimum value approach 0 when the arc length is less than 0.5 and then reach the maximum approach of 3 when the arc length is more than 0.5. Figure 8 explains the average Nu with Ra at various nanofluid volume fractions. The value of the Nusselt number increases when the nanoparticle volume fraction is increased because of an increase in the thermal conductivity, viscosity, and density of the nanofluid. Figure 9 shows Nu with Da at various nanofluid volume fractions; when the nanofluid is increased, an increase in the Nusselt number is observed. In addition, an increased Darcy number causes the Nusselt number to increase as well due to an increase in the thermal conductivity, viscosity, and density of the nanofluid.

Figure 7. Local Nusselt number along the adiabatic circular cylinder at various volume fractions at Ra = 10^6, Da = 0.001, and Yp = 0.8

Figure 8. Average Nu with Ra at various nanofluid volume fractions

Figure 9. Average Nu with Da at various nanofluid volume fractions

Figure 10. Average Nu with Ra at different Da numbers

Figure 11. Local Nusselt Number along the adiabatic circular cylinder at various volume fractions at Ra = 10^6, Da = 0.001, Yp = 0.2, 0.5 and 0.8

4. CONCLUSIONS

On the basis of an overview of the results, the following items can be concluded:

- When the Darcy number is increased from Da = 10^{-5} to Da = 0.01, the maximum absolute value of the stream function improves.
- When the Rayleigh number is increased from Ra = 10^3 to Ra = 10^6, the maximum absolute value of stream function increases.
- At high Rayleigh numbers, values of the natural convection and buoyancy force become dominated, which leads to an increasing stream function.
• The maximum absolute value of the isothermal lines become denser around the heat source. Thus, the value will reach its maximum at the hot wall and its minimum at the cold wall.
• When the thickness of the boundary layer around the heat source decreases, the heat transfer rate is enhanced owing to the aggregation of isothermal lines.

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И.М. Абед, А. Абдалкасим, Р.А. Хамза,
Х.К. Хамза, Ф.Х. Али

Нумеричким поступком се истражује довођење
tоплоте природним путем за кружни цилиндар са
адијабатским зидовима који је смештен унутар
трапезоидног кућишта испуњеног нанофлуидом на
бази сребрне воде, суперпонираним са слојем заси-
ћеног порозног нанофлуида. Зид на дну кућишта се
dелимично загрева изотермном високом темпера-
tуром а изотермна ниска температура се одржава на
зиду на врху кућишта.

Техника конечних елемената се користи за нуме-
рично израчунавање бездимензионих Навијер-Сток-
сових јединица нанофлуида и порозног нанофлуида
између цилиндра и кућишта. Прецизност програма
је проверена поређењем резултата за струјнице и
изотерме добијених нумеричким путем са резул-
tатима Кима и сар. (2008). Утврђен је висок степен
слагања између резултата добијених у овом раду и
резултата Кима и сар. Истраживање је обухватало
следеће параметре: Рејлијев број, Дарсијев број,
запремински удео наночестица и дебљину порозног
слоја.