$^{13}$C$^{17}$O suggests gravitational instability in the HL Tau disc

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ABSTRACT

We present the first detection of the $^{13}$C$^{17}$O $J = 3–2$ transition toward the HL Tau protoplanetary disc. We find significantly more gas mass (at least a factor of ten higher) than has been previously reported using C$^{18}$O emission. This brings the observed total disc mass to $0.2 \, M_\odot$, which we consider to be a conservative lower limit. Our analysis of the Toomre $Q$ profile suggests that this brings the disc into the regime of gravitational instability. The radial region of instability (50–110 au) coincides with the location of a proposed planet-carved gap in the dust disc, and a spiral in the gas. We therefore propose that if the origin of the gap is confirmed to be due to a forming giant planet, then it is likely to have formed via the gravitational fragmentation of the protoplanetary disc.

Key words: stars: pre-main-sequence, individual: HL Tau – protoplanetary discs – techniques: interferometric – submillimetre: planetary systems

1 INTRODUCTION

The early phases of protoplanetary disc evolution set the initial conditions for planet formation. There is increasing evidence that the processes that lead to planet formation happen quickly (e.g. the growth of dust grains; Harsono et al. 2018), and there is now evidence for fully-assembled protoplanetary systems in young discs (~1 Myr; Clarke et al. 2018; Flagg et al. 2019). Characterising the properties of these discs in detail is essential if we are to understand the early evolution of young stars and systems of planets.

HL Tau is located in the nearby (140 pc) Taurus-Auriga star forming region (Rebull et al. 2004). Analysis of optical spectra classifies HL Tau as spectral type K5 ± 1 (White & Hillenbrand 2004), and spectral energy distribution (SED) modelling shows it to be a Class I–II protostar surrounded by both a circumstellar disc and envelope (Robitaille et al. 2007). The estimated visual extinction toward HL Tau is large, with $A_V > 24$ (Close et al. 1997). It also appears to be accreting at a high rate ($\dot{M} \sim 10^{-7} \, M_\odot \, yr^{-1}$, Beck et al. 2010). This observational evidence makes HL Tau an example of an embedded, disc-hosting star with a young age (~1 Myr, Briceño et al. 2002).

HL Tau has therefore become a prime target for studies aiming to characterise young discs (Greaves et al. 2008; Carrasco-González et al. 2009). In particular, HL Tau was the first circumstellar disc observed with the long base-

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2 OBSERVATIONS

HL Tau was observed by ALMA in Band 7 on the 24th of November 2017 for 1.46 hours with 49 antennae in configuration C43-8 under project code 2017.1.01178.S (P.I. E. Humphreys). Baseline lengths ranged from 92–8547 m, and the spectral window (SPW) covering the $^{13}$C$^{17}$O $J = 3$–2 transition (321.852 GHz) had a native spectral resolution of 0.908 km s$^{-1}$ (which we note does not resolve the $J = 3$–2 hyperfine structure).

Data (self-)calibration and imaging were performed with CASA version 5.1.1 (McMullin et al. 2007). Continuum subtraction was performed in the $uv$-plane using a constant baseline (fitorder 0). Line imaging was performed with the CLEAN algorithm, using a Keplerian mask with the measured position and inclination angles of the disc (e.g. PA = 138° and $i = 46°$; ALMA Partnership et al. 2015). The native resolution of the data resulted in a natural beam size of 0".14 × 0".11 (−13°). We used a 0".2 $uv$-taper, which was found to maximise the signal-to-noise (S/N) of the line emission, resulting in a final beamsize of 0".28 × 0".24 (−36°). The emission is detected across 9 (1.0 km s$^{-1}$) channels with a rms of 4 mJy beam$^{-1}$ per channel from the line-free channels and a peak line emission of 30 mJy beam$^{-1}$ per channel (S/N of 7.5).

3 RESULTS

Figure 1 shows the ALMA Science Verification Band 7 (~345 GHz) continuum image alongside our $^{13}$C$^{17}$O $J = 3$–2 Keplerian-masked integrated intensity (zeroth moment) map and the $^{13}$C$^{17}$O $J = 3$–2 intensity-weighted velocity (first moment) map made with a 2.5 $σ$ clip. Also shown are the de-projected and azimuthally averaged $^{13}$C$^{17}$O $J = 3$–2 integrated intensity and 0.9 mm continuum profiles derived from our dataset, binned to the same radial resolution.

The $^{13}$C$^{17}$O emission is detected out to approximately 140 au from the central star, with a velocity pattern that consistent with observations of other gas tracers (e.g. ALMA Partnership et al. 2015). There appears to be a deficit of emission (seen in both the integrated intensity map and radial emission profile) at approximately 50 au. This feature is not coincident with any substructure in the dust continuum or molecular gas (e.g. CO, HCO$^+$; Yen et al. 2016) observed at higher spatial resolution than our data. Multi-wavelength continuum observations have shown that the optical depth of the HL Tau disc at frequencies comparable to the $^{13}$C$^{17}$O $J = 3$–2 transition (~330 GHz) is high, with $τ ≈ 8$ between 40–50 au (Carrasco-González et al. 2019).

This deficit of emission is therefore likely due to the high continuum opacity at Band 7 obscuring the line emission originating from the midplane, rather than a bona-fide gap in the disc. The central peaking of the $^{13}$C$^{17}$O profile may indicate that the line emission at radii < 10 au becomes opti-
4 ANALYSIS

4.1 Conversion of line flux to disc gas mass

We use the $^{13}$C$^{17}$O observations in order to indirectly measure the total gas mass of the disc. In our previous study of the HD 163296 disc we performed 2D radiative transfer models of multiple CO isotopologues and transitions using a well tested 2D physical structure (Booth et al. 2019). Many molecular line observations toward HL Tau are significantly affected by absorption and complex velocity gradients from the surrounding cloud (see, e.g., ALMA Partnership et al. 2015; Yen et al. 2019), meaning a similar wealth of observational data is not readily available. We therefore employ a simpler method of analysis.

The HL Tau mm-dust surface density distribution has been shown to follow a power-law distribution:

$$\Sigma(r) = \Sigma_0 \left(\frac{r}{r_c}\right)^{-\gamma} \exp \left(\frac{r}{r_c}\right)^2 \times \gamma .$$

with

$$\Sigma_0 = (2 - \gamma) \frac{M_{\odot}}{2\pi r_c} \exp \left(\frac{r_m}{r_c}\right)^2 \times \gamma ,$$

where the total disc mass is 0.105 $M_{\odot}$ (assuming a gas-to-dust mass ratio of 100). $r_c$ is 80 au, $r_m$ is 8.78 au and $\gamma$ is -0.20 (Kwon et al. 2015). This model is shown in Figure 2 as the grey dashed line. Although the observed emissivity profiles of the millimetre and centimetre sized dust are more complex, the above profile has been shown to be consistent with these (Pinte et al. 2016) and there is no evidence that these features are also present in the bulk gas distribution. We therefore utilise this profile in our analysis.

A range of midplane temperature profiles exist for the HL Tau disc (e.g. Kwon et al. 2015; Zhang et al. 2015; Okuzumi et al. 2016; Carrasco-González et al. 2019). The model from Kwon et al. (2015) is consistent with a $T_{\text{mid}} = 55 \text{K}(r/10 \text{au})^{-0.65}$ for $r > 10$ au. While this is colder than other temperature structures (e.g. Zhang et al. 2015), warmer models have no CO snowline ($\sim 20$ K) within the radial extent of the disc. This is in tension with recent observations of a chemical tracer of the CO snowline, N$_2$H$^+$, which has been detected in the HL Tau disc (C. Qi, priv. comm.). We therefore utilise the above temperature structure, which places the midplane CO snowline at approximately 50 au.

We convert the observed integrated line intensity of $^{13}$C$^{17}$O to a column density of $^{13}$C$^{17}$O under the assumption of both local thermodynamic equilibrium (LTE) and optically thin line emission. For each point in the radial profile we calculate

$$N(^{13}$C$^{17}$O) = 2.04 \int I_r dv Q_{\text{int}} \exp(E_v/T_{\text{ex}}) \frac{\theta_d \theta_b}{\nu^3(S_{\mu}^2)} \times 10^{20} \text{ cm}^{-2} ,$$

where $\int I_r dv$ is the integrated line intensity in Jy beam$^{-1}$ km s$^{-1}$, $\theta_d$ and $\theta_b$ are the semi-major and semi-minor axes of the synthesized beam in arcseconds, $T_{\text{ex}}$ is the excitation temperature in K, and $\nu$ is the rest frequency of the transition in GHz (Remijan et al. 2003). The partition function ($Q_{\text{int}}$), upper energy level ($E_u$, in K), and the temperature-independent transition strength and dipole moment ($S_{\mu}^2$, in debyes$^2$) are taken from the CDMS database (Müller et al. 2005).

Since the innermost regions of the $^{13}$C$^{17}$O emission are affected by continuum absorption, we concentrate our efforts toward reproducing the level of emission between 90–110 au. As this radial location is beyond the model midplane CO snowline, any emission will be tracing CO gas from the molecular layer down to the CO snow surface (see Miotello et al. 2014). We therefore adopt $T_{\text{ex}} = 25$ K for the excitation temperature in this region (see Akiyama et al. 2012), but note that a range of values for this parameter (20–80 K) result in values of column density that are well within the observed error in the integrated intensity profile.

To convert from $^{13}$C$^{17}$O to $^{12}$C$^{16}$O we assume isotope ratios consistent with the ISM, $n(^{12}$C$^{16}$O)/$n(^{13}$C$^{17}$O) = 69, $n(^{12}$C$^{16}$O)/$n(^{12}$C$^{13}$O) = 557, and $n(^{12}$C$^{18}$O)/$n(^{12}$C$^{17}$O) = 3.6 (Wilson 1999). We then extrapolate to a $H_2$ column density assuming a moderately-depleted disc averaged $n(^{12}$C$^{16}$O)/$n(H_2)$ ratio of $5 \times 10^{-5}$. A total gas density is then calculated assuming 80% of the gas mass lies in $H_2$ (e.g Rosenfeld et al. 2013).

Based on the above, we find that an increase in the total gas mass to $M_{\text{gas}} = 0.20 \pm 0.06$ $M_{\odot}$ is required to match the observations between 90–110 au (where errors are propagated from the observed radial intensity profile). The resulting curve is shown in Figure 2 alongside our gas surface density values derived from the radial intensity profile of $^{13}$C$^{17}$O.

4.2 Assumptions influencing the derived gas mass

The conversion of line flux to gas mass depends on several assumptions, which we discuss here. Our derived gas mass is sensitive to the chosen conversion factor between CO and $H_2$ (see Bergin & Williams 2018, for a review). While
this factor is often taken to be $10^{-4}$; studies of individual protoplanetary discs have revealed carbon depletion from factors of five to orders of magnitude (e.g. McClure et al. 2016), and surveys have demonstrated this phenomenon is widespread (e.g. Miotello et al. 2017). Our chosen value of $n(^{13}\text{C}^{17}\text{O}) / n(\text{H}_2) = 5 \times 10^{-5}$ therefore accounts for a modest depletion factor of two, in agreement with disc chemical models at ages of $\sim 1$ Myr (Schwarz et al. 2018; Bosman et al. 2018)\footnote{Though we note depletion factors depend on variables such as temperature and ionisation rate.}. The derived disc gas mass scales linearly with the inverse of the depletion factor, so under the assumption of no carbon depletion (e.g. $10^{-4}$), our derived disc mass would be half our quoted value.

We have also assumed that our observations trace the full column of CO on both the ‘near’ and ‘far’ sides of the disc. This will not be the case if (i) there is a significant fraction of CO frozen out in the disc midplane, or if the $^{13}\text{C}^{17}\text{O}$ J = 3–2 emission is optically thick. In addition (as discussed in Section 3), Carrasco-González et al. (2019) have determined that the continuum optical depth in the disc is high, with $\tau \sim 8$ at 330 GHz. Therefore, our observations are not sensitive to CO emitting on the far side of the disc. In this scenario, the true gas mass in the disc would be (at least) a factor of two higher.

Observations of CO rovibrational lines toward the HL Tau envelope have revealed a significantly higher fraction of CO frozen out in the disc midplane, or if the $^{13}\text{C}^{17}\text{O}$ J = 3–2 emission is optically thick. In addition (as discussed in Section 3), Carrasco-González et al. (2019) have determined that the continuum optical depth in the disc is high, with $\tau \sim 8$ at 330 GHz. Therefore, our observations are not sensitive to CO emitting on the far side of the disc. In this scenario, the true gas mass in the disc would be (at least) a factor of two higher.

The precise magnitude of these effects cannot be determined without dedicated modelling of the HL Tau disc.

Nevertheless, we believe our estimates for these factors imply that our derived gas mass is a conservative lower limit. Future high spatial and spectral resolution observations of multiple CO isotopologues toward HL Tau will enable us to place more stringent constraints on the gas mass in the disc.

5 DISCUSSION

5.1 Comparison to other mass measurements

Tapia et al. (2019) use combined dust and gas evolutionary disc models to reproduce ALMA and VLA continuum profiles of the HL Tau disc from to 0.87–7.8 mm. Their best fitting model possesses a dust mass of $4.8 \times 10^{-3} M_\odot$, which is between a factor of 50–100 smaller than the gas mass implied by our results. However, the above work adopts $\text{CO} / \text{H}_2$ ratio of $2.7 \times 10^{-4}$, which assumes no C depletion, and that all potential volatile carbon in the disk is the form of CO (given an ISM C/H ratio of $1.4 \times 10^{-4}$; Cardelli et al. 1996). If we adopt the same ratio as Wu et al. (2018), our resulting gas mass would be $\sim 0.04 M_\odot$, which is still a factor of 10–200 higher than the gas mass derived from $^{13}\text{C}^{17}\text{O}$.

Using Equation 3 we can compare the values for $N(^{13}\text{C}^{17}\text{O})$ and $N(^{12}\text{C}^{18}\text{O})$. A column density ratio of $\sim 250$ would imply that both lines are optically thin. However, using our data and the data from the radial profile presented in (Wu et al. 2018) for a radius of 100 au, we find that the ratio is only $\sim 4$. This demonstrates that the $^{18}\text{O} J = 2–1$ emission is optically thick in the HL Tau disc, and is therefore not tracing the bulk gas mass in the molecular layer (as also found for HD 163296; Booth et al. 2019).
5.2 The (in)stability of the disc

The gravitational stability of the higher mass disc can be assessed using the Toomre $Q$ parameter (Toomre 1964),

\[ Q = \frac{c_s \kappa}{\pi G \Sigma} \]

(4)

where $c_s$ is the sound speed of the gas (calculated from $T_{\text{mid}}$), $\Sigma$ is the surface density of the gas and dust, and $\kappa$ is the epicyclic frequency (equal to the angular velocity $\Omega$ in a Keplerian disc where we assume a central star mass of $\sim 1.7$ $M_\odot$, Pinte et al. 2016). The resulting radial profile of $Q$ is shown in Figure 3a.

Regions of the disc with $Q \lesssim 1.7$ will be susceptible to gravitational instability (Durisen et al. 2007; Helled et al. 2014), leading to non-axisymmetric structure in the disc and potentially fragmentation. Our observations therefore support a picture in which the disc around HL Tau is gravitationally unstable ($Q < 1.7$) from approximately 50–110 au (with minimum $Q \approx 1.1 \pm 0.2$ at $r = 77$ au). Taking into account observational uncertainties, it is also possible that $Q < 1$ between 60–100 au.

If the disc around HL Tau is threaded by a magnetic field, then this may offer an additional mechanism to support the disc against self-gravity. In these cases, $Q$ is modified by a factor $\sqrt{1+1/\beta_p}$ (where $\beta_p$ is the plasma parameter) and the threshold for instability lies within the range $Q \lesssim 1.2$–1.4 (Kim & Ostriker 2001). In general, values of $\beta_p$ range from $\sim 10$ under ideal MHD conditions (Forgan et al. 2017) up to $10^8$ for non-ideal MHD (Hasegawa et al. 2017). Such values do not alter our minimum Toomre $Q$ value by more than $\pm 5$ per cent, suggesting that even if the HL Tau disc possesses a strong magnetic field ($\beta_p \sim 10$), it would not be sufficient to move the disc into a stable regime.

5.3 The region of instability in context

Figure 3b shows the region of instability in the HL Tau disc with respect to the Band 7 (0.9 mm) continuum observations of ALMA Partnership et al. (2015). The unstable region spans several of the bright rings and dark gaps identified in the dust disc (B3–B7 and D4–D7). Modelling of unstable discs with a decoupled dust component shows grains concentrating in spiral arms (e.g. Rice et al. 2004; Dippierro et al. 2015a). Therefore it is not immediately clear how to reconcile such an apparently unstable disc with the ordered concentric rings observed in the dust.

Several studies have shown that the ‘double gap’ feature from $\sim$65–74 au (D5–B5–D6) can be reproduced by the presence of a planet with mass between $\sim 0.2$–$0.6$ $M_{\text{Jup}}$ (Dippierro et al. 2015b; Jin et al. 2016; Dong et al. 2018), which is supported by mm–cm observations across this radial region (Carrasco-González et al. 2019). The higher gas surface density revealed by our observations implies that mm-sized grains would be better coupled to gas than in the above works. Therefore, larger planet masses would be required to match the observed dust structures. When considering the lower bound of our observational errors, we find $Q \lesssim 1$ from $\sim$60–100 au. Here the local cooling time is expected to be short (e.g. Rafikov 2005; Clarke & Lodato 2009), meaning that this region of the disc would undergo gravitational fragmentation. This scenario is in agreement with dedicated modelling of star-disc systems with similar properties as HL Tau, which form fragments with masses between 1–5 $M_{\text{Jup}}$ (Boss 2011). Therefore, if such a planet is confirmed to be the origin of this observed gap structure, then we suggest it has likely formed via gravitational fragmentation.

Recently, Yen et al. (2019) detected a spiral feature in observations of HCO$^+$ $J = 3–2$ toward HL Tau. While they attribute the spiral to in-falling material from the surrounding envelope, this feature crosses our region of instability in the disc. Chemical models of gravitationally unstable discs have predicted HCO$^+$ to be a tracer of spiral structure (Ilee et al. 2011; Douglas et al. 2013). In light of this, we suggest that the spiral structure on small ($\lesssim$100 au) scales could be due to gravitational instability within the disc.

6 CONCLUSIONS

We have presented the first detection of $^{13}$C$^{17}$O in the HL Tau disc, revealing a significant reservoir of previously hidden gas mass. The total disc mass is now sufficient for the disc to be considered gravitationally unstable between 50–110 au. This region crosses a spiral feature observed in the gas, and a proposed planet-carved gap in the dust continuum. We suggest that if a massive planet is confirmed to be the origin of this gap, then it likely formed via gravitational fragmentation of the protoplanetary disc.

This work represents only the second detection of $^{13}$C$^{17}$O in a protoplanetary disc. It further demonstrates the utility of rare CO isotopologues in probing the physical conditions in discs, with important implications for their evolution and the formation of planets within them.

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