Mass Transport in Catalytic Pores of GDE-Based CO2 Electroreduction Systems

Divya Bohra, Jehanzeb Chaudhry, Thomas Burdyny, Evgeny Pidko, Wilson Smith

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Mass transport in catalytic pores of GDE-based CO$_2$ electroreduction systems

Divya Bohra,† Jehanzeb H. Chaudhry,‡ Thomas Burdyny,† Evgeny A. Pidko,¶ and Wilson A. Smith*,†.§.∥

†Materials for Energy Conversion and Storage (MECS), Department of Chemical Engineering, Delft University of Technology, Delft, The Netherlands
‡Department of Mathematics and Statistics, University of New Mexico, Albuquerque, USA
¶Inorganic Systems Engineering (ISE), Department of Chemical Engineering, Delft University of Technology, Delft, The Netherlands
§Department of Chemical and Biological Engineering, University of Colorado Boulder, Boulder, USA
∥National Renewable Energy Lab, Golden, USA

E-mail: wilson.smith@colorado.edu

Abstract

Gas diffusion electrode (GDE)-based setups have shown promising performance for CO$_2$ electrocatalysis and further development of these systems will be important on the path to industrial feasibility. In this article, we model an effective catalyst pore within a GDE-based flow-cell to study the influence of the catalyst structure and operating conditions on the reaction environment for CO$_2$ electrocatalysis at practically relevant current densities. Using a generalized modified Poisson-Nernst-Planck (GMPNP) 3D model of the nanoporous catalyst layer, we show that the length of the catalyst pore as well as the boundary conditions at the gas-electrolyte and electrolyte-electrolyte interfaces across this length are highly influential parameters for determining the conditions
within the catalyst pore. Pores with the same catalytic surface area can have very different reaction environments depending primarily on the pore length and not the pore radius. Properties such as electrolyte pH and buffer breakdown, ionic strength and CO₂ concentration are also highly-sensitive to the catalyst layer thickness, gas pressure, electrolyte flow rate and the flow-channel geometry. The applied potential impacts the concentration of ionic species in the pore, which in turn determines the solubility of CO₂ available for the reaction. Our results underline the need to understand and manage transport within GDE-based electrocatalysis systems as an essential means to control catalyst performance. Benchmarking of GDE-based electrocatalytic systems against their structural and operational parameters will be important for achieving improvements in performance that can be ultimately translated to large-scale operation.

**Introduction**

The solubility of carbon dioxide (CO₂) in aqueous electrolytes under ambient conditions is ~ 33 mM. In a system design where the electrolyte is saturated with dissolved CO₂, mass transport limits the achievable CO₂ reduction current density to below 50 mA/cm² irrespective of the nature of the catalyst employed.¹⁻¹¹ For the process to be economically feasible, current densities in the order of ~ 200 mA/cm² and greater are estimated to be required in addition to the selectivity, over-potential and stability targets.¹²⁻¹⁴ Gas diffusion electrodes (GDE) based cell designs have been demonstrated to successfully overcome this mass transfer limitation in CO₂ electrochemical reduction (eCO₂R) systems.¹⁵⁻²¹

The classical GDE-based eCO₂R systems studied in literature are flow-cells or microfluidic cells following a general setup as shown in Figure 1a for the cathode half of the reactor.²²⁻³¹ The GDE cathode itself is typically composed of 3 layers: 1) the gas diffusion layer (GDL) which acts as a gas distribution network for the incoming CO₂ and outgoing gaseous products to and from the catalyst, 2) a thin micro-porous layer (MPL) of carbon nanoparticles deposited on the GDL which acts as the current collector and 3) the electrocatalyst layer
Figure 1: (a) Illustration of a typical cathode setup in a GDE-based flow-cell for CO$_2$ reduction. The green and the blue zones signify the gas and the aqueous phase, respectively. The dotted arrows represent the general direction of the flow. GDL: gas diffusion layer, MPL: micro-porous layer, CL: catalyst layer, BL: boundary layer, $L_{cross}$: cross-sectional width of the liquid flow channel, $A_{cross}$: perpendicular cross-sectional area of the liquid flow channel. (b) Zoomed-in illustration of the effective cylindrical pore used as the model system. $S_1$, $S_2$ and $S_3$ are the simulation domain boundary surfaces and represent the gas-electrolyte interface at the pore entry, the cylindrical catalyst surface and the electrolyte-electrolyte interface at the pore exit, respectively. $R$ is the pore radius and $L$ is the pore length. $r$, $z$ and $\Theta$ represent the radial, longitudinal and azimuthal axes, respectively. $J_i$ stands for the flux of species $i$ normal to the respective surface.

During operation of a GDE, a gas stream of pure CO$_2$ flows from the inlet of a channel along the GDL, leaving the gas channel with the gaseous products of the catalysis. Similarly, a liquid flow channel facing the catalyst of the GDE continuously circulates the aqueous electrolyte. The diffusion length of CO$_2$ to the catalyst surface in such a setup is several orders of magnitude smaller than in a system where the CO$_2$ dissolved in the bulk electrolyte has to diffuse to the cathode surface (from here-on referred to as an H-cell type setup), resulting in a drastic improvement in the achievable current density attributed to eCO$_2$R. There are
practical advantages to electrolyte-flow systems that make them a desirable setup for studying and optimizing eCO$_2$R such as: a higher control of reaction conditions and therefore catalyst selectivity and activity through the composition of the electrolyte, better water management for the catalysis and for membrane stability, and ease of liquid product sampling due to continuous flow.

Other system configurations such as membrane-electrode assemblies (MEA) inspired by fuel cell architectures have been proposed in literature as an alternative to flow-cells. MEAs reduce the impacts of flooding due to the elimination of liquid electrolyte flow, and can potentially achieve even higher eCO$_2$R current densities due to better access to CO$_2$ from the gas phase. These advantages make MEA setups an attractive candidate for systems operating at practically relevant scales. However, controlling product selectivity, water management, salt precipitation-related fouling as well as membrane stability can be a challenge in these setups. There is considerable variation in the cell-design and performance analysis among the initial MEA studies, making a comparison between the different approaches difficult. Further systematic studies are required to establish best design and operational practices for optimal performance for the respective eCO$_2$R products.

In this report, we will focus on modeling the mass transport within the CL in flow-cell type systems as depicted in Figure 1a. As the number of experimental studies using GDE-based flow-cells increase, there is a rising need to compliment these with simulations to better understand the effect of the various system parameters on the measured performance. The porous nature of the catalyst layer in the flow-cell systems are much more complex than the H-cell setups that have been modeled extensively in literature so far, making it difficult to isolate and experimentally measure the effects of the various parameters. At substantial current densities, the structure, porosity, exposed surface area and width of a deposited catalyst layer will impact the environment of a CL pore network, necessitating the consideration of catalyst structure when interpreting experimental electrochemical performance. Additionally, flow-cells present several design and operational handles to influence reaction
Electrolyte composition and pH within the catalyst layer of the GDE is understood to be an influential parameter for the selectivity of CO\textsubscript{2} reduction.\textsuperscript{21} Multiple experimental studies using flow-cells observe a correlation between the electrolyte and C-C coupling reaction on Cu catalysts to form ethylene,\textsuperscript{22,27,28} CO Faradaic efficiency on Ag\textsuperscript{24–26,31} and formate production on Sn.\textsuperscript{29} An optimal control of the reaction environment is expected to have a dramatic influence on the catalyst performance as has also been observed in studies in H-cell setups.\textsuperscript{46–52} Previously reported models pertaining to GDE flow-cell configurations assume a one-dimensional (1D) structure-less approach to simulating transport within the flow-cell CL.\textsuperscript{27,53–55} Here we simulate the reaction environment within an effective three-dimensional (3D) catalytic pore of a GDE-based flow-cell to understand the influence of changing pore structure and boundary conditions on the electrolyte composition during steady-state operation at practically relevant current densities (> 50 mA/cm\textsuperscript{2}, see Figure 2b). We use the generalized modified Poisson-Nernst-Planck (GMPNP) model\textsuperscript{56,57} as reported recently by us for a 1D H-cell setup case,\textsuperscript{43} and extend it for 3D cylindrical pores with appropriate boundary conditions relevant for laboratory flow-cell setups.

Our analysis of the GDE flow-cell finds that the length is one of the most influential structural parameters of the catalyst layer for the median pH and ion concentration within the pore. The length of the pore becomes an important parameter due to the fact that the fluxes of species at the gas-electrolyte and electrolyte-electrolyte interface are large enough to compete with the rates of the reactive and diffusive processes within the pore. As a result, the boundary conditions for the catalyst layer such as the gas pressure and the electrolyte flow rate play a very important role in determining optimal reaction conditions for the catalyst. By comparing the performance of the GMPNP model with a reaction-diffusion model, we discuss the relevance of the applied potential for ionic concentration, CO\textsubscript{2} solubility and edge effects within the pore. GDE-based flow-cells are characterized by a narrow and porous catalyst layer surrounded by interfaces that have a major influence on transport of species
in and out of the reactive domain. The reaction environment in GDE setups is expected to deviate significantly from what is encountered in eCO$_2$R in H-cell setups and therefore a considerably different performance with respect to onset-potential, selectivity and activity can be expected.

**Model description**

Figure 1b illustrates the cylindrical pore domain used for the GMPNP simulation. This is an idealization of the CL for the purposes of deduction. The pore structures in the actual CL deposited on the GDL are expected to be highly heterogeneous as reported in a very recent tomography study on Ag GDE cathode.$^{58}$ We assume the catalytic pore to be completely flooded with electrolyte such that the gas-electrolyte interface is located at the pore entry (the boundary between the MPL and CL, $S_1$). We believe that this is a reasonable assumption for a metal catalyst pore with small radii at a reducing potential and that a vast majority of current density in flow-cell systems can be attributed to the double-phase electrolyte-catalyst boundary ($S_2$) like in case of an H-cell. We use CO producing catalysts as a test case for our simulations due to the prevalence of several experimental studies using GDEs showing promising results for CO$_2$ reduction to CO.$^{59-62}$ The following sections discuss the boundary conditions assumed at $S_1$, $S_2$ and $S_3$ in detail. The values of the constants used in the model can be found in the Parameters section in the SI. Parameters depicted in bold lettering imply vectors.

**Gas-electrolyte interface ($S_1$)**

The surface $S_1$ represents the gas-electrolyte interface located at the boundary between the MPL and the catalyst layer. The gas phase is assumed to be composed of 95% CO$_2$, 4.5% carbon monoxide (CO) and 0.5% hydrogen (H$_2$) and the pressure at $S_1$, $p_1$ is assumed to be 1 bar. We have ignored the presence of humidity in the gas stream and evaporation of the
The gas phase composition for CO producing GDE setups have not been reported for experimental setups in literature. For this reason we assume the gas phase to consist of a high % of CO$_2$ based on the fact that single-pass conversion efficiency for eCO$_2$R is typically low for lab-scale flow-cells. In practice, several factors such as the incoming gas-phase CO$_2$ flow rate, the Faradaic efficiency of CO$_2$ reduction, the current density and the transport characteristics of the GDL and rate of the flux of the product gases across the gas-electrolyte interface will determine the steady-state composition at $S_1$. For the model, the interface $S_1$ is considered to be in equilibrium and Dirichlet boundary conditions are assumed for CO$_2$, CO and H$_2$ concentrations at $S_1$ as per the equation (1). The assumption of equilibrium at the gas-liquid interface is valid in the majority of situations, except when very high mass transfer rates are present at the interface. This can possibly be the case for the flux of the product species CO and H$_2$ across $S_1$ which are present in low concentrations in the gas phase and have relatively low solubility in the electrolyte. This is not seen as an issue for resolving the reaction environment within the pore, since, in addition to their low solubility, CO and H$_2$ do not interact with the electric field nor participate in the homogeneous reaction kinetics. Such factors require further attention for multi-carbon product formation where aqueous CO concentrations are expected to be important.

$$C_{i}^{S_1} = H_i p_1 y_i \rho_e$$  \(1\)

where $H_i$ is Henry’s constant for species $i$ (in mol·kg$^{-1}$·bar$^{-1}$), $p_1$ is the gas phase pressure at $S_1$ (in bar), $y_i$ is the mole fraction of $i$ at $S_1$, $\rho_e$ is the density of the electrolyte (assumed as water density, not adjusted for ion concentration for simplicity, in kg·m$^{-3}$ at 25°C) and $C_{i}^{S_1}$ is the concentration of species $i$ at $S_1$ (in mM). $H_{CO_2}$ is calculated using Sechenov equation$^{64,65}$ (see section Model details in the SI) to account for the effect of ion concentrations in the pore. Median values of ion concentrations in the pore are used at every time step to iteratively adjust the value of $H_{CO_2}$ to determine the Dirichlet condition at $S_1$. The fluxes ($J_i$) of all
species except CO$_2$, CO and H$_2$ are considered to be 0 at $S_1$ (no-flux boundary condition). Dirichlet boundary condition is used for the potential at $S_1$ as given in equation (3).

$$J_{HCO_3^-\text{,CO}_2^2^-\text{,K}^+,\text{H}^+,\text{OH}^-}\mid_{z=0,x,y,t} = 0 \quad (2)$$

$$\phi\mid_{z=0,x,y,t} = 0 \quad (3)$$

**Catalyst surface ($S_2$)**

The following heterogeneous reactions are considered to be occurring at the cathode surface $S_2$ during eCO$_2$R. We assume CO producing catalysts such as Ag/Au as our test case.

$$\text{CO}_2(aq) + \text{H}_2\text{O} + 2e^- \rightleftharpoons \text{CO}(g) + 2\text{OH}^- \quad (4)$$

$$2\text{H}_2\text{O} + 2e^- \rightleftharpoons \text{H}_2(g) + 2\text{OH}^- \quad (5)$$

A total current density ($I_{\text{total}}$) and Faradaic efficiency (FE) distribution (ratio of electrons consumed for H$_2$ production vs CO) is assumed for the simulations. $I_{\text{total}}$ is assumed to be either normalised by the electrochemically active surface area ($I_{\text{ECSA}}$) or the geometrical surface area ($I_{\text{geom}}$) which will be defined later in this section. No direct consumption of H$^+$ is assumed since the associated current will be negligible especially at the high current densities associated with flow-cells. The flux of the solution species at the surface is given by the equations (6) - (10). $r=R$ in our simulations is assumed to be the outer Helmholtz plane (OHP) since there is no charge density in the Stern layer by definition. The factor of 0.5 in the equations (7) - (9) comes from the product to electron stoichiometry of the reactions (4)
We assume no bubble formation of the product species within the catalyst pore and therefore also no convection or turbulence effects within the pore due to bubbling.

\[ J_{HCO_3^-} |_{\sqrt{x^2+y^2}=R,z,t} = 0 \]  

\[ J_{CO_2} |_{\sqrt{x^2+y^2}=R,z,t} = 0.5 \times \frac{I_{total}}{F} \times FE_{CO} \]  

\[ J_{CO} |_{\sqrt{x^2+y^2}=R,z,t} = -0.5 \times \frac{I_{total}}{F} \times FE_{CO} \]  

\[ J_{H_2} |_{\sqrt{x^2+y^2}=R,z,t} = -0.5 \times \frac{I_{total}}{F} \times FE_{H_2} \]  

\[ J_{OH^-} |_{\sqrt{x^2+y^2}=R,z,t} = -\frac{I_{total}}{F} \]  

where \( F \) is the Faraday’s constant and \( FE_{CO} \) and \( FE_{H_2} \) are assumed to be 95\% and 5\%, respectively. Dirichlet boundary condition is used for the potential at \( S_2 \) as given in equation (11) where \( V_{app} \) is the applied voltage in V.

\[ \phi |_{\sqrt{x^2+y^2}=R,z,t} = V_{app} \]  

**Electrolyte-electrolyte interface (\( S_3 \))**

We assume an electrolyte concentration of 1 M KHCO\( _3 \) as the bulk solution with the electrolyte flow parallel to the catalyst surface with a flow velocity \( v_e \) in \( m^3 \cdot s^{-1} \). The flux of species \( i \) across the surface \( S_3 \) is assumed to depend linearly on the concentration gradient between \( S_3 \) and the bulk electrolyte solution as per the equation (12). We have assumed a very small concentration (1 \% of equilibrium concentration at \( S_1 \)) of CO and H\( _2 \) in the bulk.
solution to be able to normalize the concentrations of both species to solve the GMPNP equations and to define the driving force for the flux in equation (12). Physically, this assumption implies that although, a majority of the CO and H\(_2\) produced leave the system through the gas-liquid interface at \(S_1\), a small quantity also moves into the bulk electrolyte through the liquid-liquid interface \(S_3\) due to diffusive and convective fluxes. The value of 1\% is arbitrarily chosen for the current simulations. Experimental data or models with more detailed treatment of CO and H\(_2\) mass transport through the system can be used to better inform the concentration of CO and H\(_2\) into the bulk electrolyte flow at steady state as a function of the operating conditions.

\[
\mathbf{J}_i^e|_{z=L_{x,y,t}} = k^e_i (C^{S_3}_i - C^0_i) \quad i = \text{CO}_2, \text{CO}, \text{H}_2, \text{HCO}_3^-, \text{CO}_3^{2-}, \text{H}^+, \text{OH}^-, \text{K}^+ \quad (12)
\]

\[
Sh = \frac{k^e_i}{D_i/L_c} = 1.017\left(\frac{2L_c}{L_{cross}}ReSc\right)^{1/3} \quad (13)
\]

\[
Re = \frac{\rho_e|v_e|L_c}{\mu_e A_{cross}} \quad (14)
\]

\[
Sc = \frac{\mu_e}{\rho_e D_i} \quad (15)
\]

where \(k^e_i\) is the convective mass transfer coefficient in m·s\(^{-1}\) derived using the Sherwood number \((Sh)\) as per equation (13).\(^{63}\) \(C^{S_3}_i\) and \(C^0_i\) are the concentrations of species \(i\) at \(S_3\) and in the bulk electrolyte, respectively (in mM). Equation (13) is applicable for laminar flow over a flat plate of length \(L_c\) (in m), which in this case, is the length of the catalyst along which the electrolyte is flowing, for an electrolyte film thickness assumed to be half of the cross-sectional width of the liquid channel \((L_{cross}/2\), in m) and a flow cross-section of \(A_{cross}\) (in m\(^2\)). \(Re\) and \(Sc\) are Reynolds and Schmidt numbers respectively and are given by equations (14) and (15). \(\rho_e\) and \(\mu_e\) are density (in kg·m\(^{-3}\) at 25\(^\circ\)C) and viscosity (in
kg·m$^{-1}$·s$^{-1}$ at 1 atm, 25°C) of the electrolyte, respectively and are assumed be that of pure water. Dirichlet boundary condition is used for the potential at $S_3$ as given in equation (16).

$$\phi|_{z=L,x,y,t} = 0$$  \hspace{1cm}  (16)

**GMPNP system of equations**

The generalized modified Poisson-Nernst-Planck (GMPNP) equations used to model the mass transport of species in the electrolyte within the cylindrical pore are analogous to the equations used in reference 43.

$$\frac{\partial C_i}{\partial t} = -\nabla \cdot J_i + \sum_j R_i$$  \hspace{1cm}  (17)

where $C_i$ is the concentration of species $i$, $t$ is time, $j$ is the index of the homogeneous reaction in solution, $R_i$ is the rate of production of species $i$ due to the homogeneous reaction $j$ as given by equations (9) to (13) in the SI and $J_i$ is the flux of species $i$ given by:

$$J_i = -D_i^{\text{eff}} \nabla C_i - \frac{D_i^{\text{eff}} C_i z_i F}{R_G T} \nabla \phi - D_i^{\text{eff}} C_i \left( \frac{N_A \sum_{i=1}^{n} a_i^3 \nabla C_i}{1 - N_A \sum_{i=1}^{n} a_i^3 C_i} \right)$$  \hspace{1cm}  (18)

$$D_i^{\text{eff}} = \frac{D_i \epsilon \delta}{\tau^2}$$  \hspace{1cm}  (19)

where $D_i^{\text{eff}}$ is the effective diffusion coefficient of species $i$ given by equation (19), $z_i$ is the charge of species $i$, $R_G$ is the gas constant, $T$ is the temperature, $N_A$ is the Avogadro’s constant and $a_i$ is the effective solvated diameter of the species $i$. In equation (19), $D_i$ is the diffusion coefficient, $\epsilon$, $\delta$ and $\tau$ are the effective porosity, constrictivity and tortuosity of the catalyst layer, respectively (assumed to be 0.5, 1.5 and 0.9, respectively). Equation (17) needs to be solved self-consistently with the Poisson equation given by:
\[ \nabla \cdot (\varepsilon_0 \varepsilon_r \nabla \phi) = -F \sum_{i=1}^{n} z_i C_i \]  \hspace{1cm} (20)

where \( \varepsilon_0 \) is the permittivity of vacuum, \( \varepsilon_r \) is the relative permittivity of the electrolyte and \( \phi \) is the potential. The relative permittivity in equation (20) is assumed to vary with cation concentration as given by equation (21).\(^{67,68}\) The concentration terms in the equation (21) are in M. \( M_{\text{water}} \) is the molarity of water at room temperature taken to be 55 M and the parameters \( w_i \) are the total number of water molecules held by the cation \( i \). \( \varepsilon_r^0 \) is taken to be 80.1 equal to the relative permittivity of water at room temperature whereas \( \varepsilon_r^{\text{min}} \) is the dielectric constant of water under the condition of dielectric saturation and is taken as 6. The scaled GMPNP equations for the 3D cylindrical pore is given in the Model details section in the SI.

\[ \varepsilon_r = \varepsilon_r^0 \left( \frac{M_{\text{water}} - \sum_{i}^{ncat} w_i C_i}{M_{\text{water}}} \right) + \varepsilon_r^{\text{min}} \left( \frac{\sum_{i}^{ncat} w_i C_i}{M_{\text{water}}} \right) \] \hspace{1cm} (21)

All species are assumed to be at their bulk concentrations at \( t=0 \) with the catalyst in a grounded state as given in equations (22) and (23).

\[ C_i|_{x,y,z,t=0} = C_i^0 \] \hspace{1cm} (22)

\[ \phi|_{x,y,z,t=0} = 0 \] \hspace{1cm} (23)

The FEniCS project\(^{69,70}\) Python package is used to solve the Galerkin (weak) form of the GMPNP equations (17) - (20) using backward Euler method for time discretization (details in the SI) over a uniform 3D cylindrical mesh.

Since we are modeling an effective catalyst pore, the current density used for the simulations should be understood as electrochemically active surface area (ECSA)-normalized current density (\( I_{\text{ECSA}} \)) and not geometrically normalized (\( I_{\text{geom}} \)). Comparing and bench-
Figure 2: (a) A cartoon illustration comparing the electrochemically active surface area (ECSA) depicted through the red outlines on the yellow catalyst vs. the geometric surface area (GSA) depicted through the blue semi-opaque projected surface on top of the catalyst layer. The grey particles represent the MPL deposited on top of the GDL as shown in Figure 1a. (b) Plot showing geometrically normalized current density ($I_{\text{geom}}$) as a function of the electrochemically active surface area-normalized current density $I_{\text{ECSA}}$ for different values of the roughness factor ($f_r$) as per equation (24).

Figure 2a illustrates the difference between the catalyst surface area relevant for estimating $I_{\text{ECSA}}$ vs. $I_{\text{geom}}$. $I_{\text{ECSA}}$ can be understood in terms of $I_{\text{geom}}$ and the catalyst roughness factor ($f_r$) as given by equation (24).

$$I_{\text{ECSA}} = \frac{I_{\text{geom}}}{f_r}$$  \hspace{1cm} (24)

McLaughlin et al.\textsuperscript{58} have recently reported surface area measurements for Ag GDE which are equivalent to a roughness factor of $\sim$ 50. $f_r$ will depend on the properties of the catalyst and the GDL/MPL layer as well as on the deposition technique and the CL thickness. Additionally, the roughness can also change due to restructuring of the catalyst during op-
eration. We use $I_{ECSA}$ values of 1 mA/cm$^2$, 2 mA/cm$^2$ and 3 mA/cm$^2$ for the simulations in this report. Figure 2b shows $I_{geom}$ as a function of $I_{ECSA}$ with $f_r$ as the slope (equation (24)), highlighting that $I_{ECSA}$ values of 1-3 mA/cm$^2$ represent experimental geometric current densities in the 100’s of mA/cm$^2$, on par with recent literature.

In the following section, we present the results for GMPNP simulations within a cylindrical pore for changing pore geometry and boundary conditions. Unlike the 1D GMPNP simulations reported in reference 43, where a wide range of potentials were simulated to study the effect on the electrical double layer (EDL), here we focus on comparing the median values of species concentrations within the catalytic pore. The 3D simulations are numerically unstable beyond a small applied potential ($V_{app}$) at the OHP of -25 mV vs potential at the point of zero charge (PZC) and require extremely small time steps to converge. This makes the simulations at higher $V_{app}$ computationally intractable. All GMPNP results reported in this article are derived for an applied potential of -25 mV vs PZC which corresponds to a surface potential of $\sim$ -0.5 V vs standard hydrogen electrode (SHE) for Ag(111) and $\sim$ -0.75 V vs SHE for polycrystalline Ag (see Parameters section in the SI). Steric effects are not expected to play an important role at small applied potentials and similar results are expected from a PNP model without any steric modifications to the flux term in equation (18). However, the GMPNP equations are numerically more stable than PNP and do not require additional numerical stabilization for convergence Bohra et al..

Lastly, based on the few attempts at measuring the pore structure properties of metal catalysts deposited on GDEs for eCO$_2$R,$^{22,58}$ the pore radii are expected to lie between 100 to 1000 nm. We have assumed a radius of 5 nm for our simulations unless otherwise stated, primarily due to computational limitations since the finite element mesh grows with $R^2$. A very fine space discretization is needed in order to resolve the EDL region close to the cylindrical surface $S_2$ using the GMPNP model. A mesh with radially variable element sizes can be used for pores with larger radii to circumvent this issue. The pore radius is not expected to influence the conclusions drawn regarding the influence of pore structure on
mean reaction conditions within the pore. However, the influence of $R$ will become prominent when studying the effect of applied potential on median reaction conditions within the pore and will be discussed further in the results section.

**Results**

In the following section, we vary different aspects of the pore structure to study its effect on the median properties of the electrolyte within the effective catalyst pore. Subsequently, we consider the effect of the model choices such as the boundary conditions in more detail and provide a comparison with the reaction-diffusion model.

**Pore structure of catalyst**

**Length of catalyst pore**

The length of the catalyst pore is a function of the thickness of the catalyst layer deposited on top of the MPL as well as the tortuosity ($\tau$) of the porous structure. We have varied the length of the model cylindrical pore $L$ in order to study its effect on the concentration of the various solution species within the pore. Catalyst layer thickness has been shown to effect the eCO$_2$R performance experimentally where the variation has been attributed to CO$_2$ concentration and the pH within the catalyst pores.$^{27}$

Figure 3a and 3b show how, as the length of the pore increases, the pH in the pore becomes more basic accompanied by a buffer breakdown seen by the depletion of HCO$_3^-$ from the pore. This dramatic increase in pH for constant $I_{ECSA}$ with increasing $L$ is a result of the relative rate of diffusion of species within the pore and their flux at the electrolyte-electrolyte interface $S_3$. The length of the pore needed for the buffer breakdown to happen goes down with increasing $I_{ECSA}$ due to a higher rate of OH$^-$ production. Another interesting consequence of increasing pore length is the build-up of cations and carbonate ions within
the pore as can be seen in Figure 3c and S1. The concentration of these charged species has an influence on the solubility of CO$_2$ within the pore as described in the model description section. The concentration of the cations and carbonate ions can also be relevant for ion precipitation within the catalyst pores which can potentially lead to fouling.$^{22,31}$ We do not assume any specific adsorption of cations on the catalyst surface in our simulations. However, an increased build-up of cations within the pores at high applied voltage can possibly result in the cations chemically adsorbing on the catalyst walls and significantly influencing catalyst activity. Although, the absolute CO$_2$ concentration does not change significantly over the
whole range of $L$ and $I_{ECSA}$ (Figure 3d), the trend shows a clear competition between the outgoing CO$_2$ fluxes at $S_2$ and $S_3$ as well as the influence of higher ion concentrations on the equilibrium concentration of CO$_2$ at $S_1$.

Figures 8b, S7b, S9a, S8b and S10 show the distribution of electrolyte species across a longitudinal cross-section of a 5 nm x 100 nm ($R \times L$) pore derived for the GMPNP model. No significant variation can be observed for the solution species along the length of the pore except for the products CO and H$_2$ which are present in a very low concentration. The species fluxes and the applied potential, however, have a clear influence on the concentration profiles along the pore boundaries. The influence of applied potential on concentration profiles follows the same general behavior as discussed in reference 43. The product gases CO and H$_2$ are assumed to be at equilibrium at the gas-liquid interface as mentioned previously. This implies that as the catalytic reaction progresses within the pore, CO and H$_2$ build up beyond their equilibrium solution concentration along the length of the pore as can be seen in Figure S10. The mass transport of gaseous product species from the flooded catalyst pore through the GDL can be much more complex than captured by the model used. However, since CO and H$_2$ are present in very low concentrations, are uncharged species and do not participate in any homogeneous reactions in the electrolyte, their mass transport within the pore can be independently resolved through more complex models that take into account possible nucleation and bubble formation. If the formation of gaseous bubbles is, in fact, a significant effect within the catalyst pores, this will in turn influence the mass transport of other species through turbulence and fluctuation of catalyst surface voltage leading to a much more complex dependence between the transport and catalyst performance.

**Surface area of catalyst pore**

Catalyst surface area is often regarded as a very important parameter for improving performance, but the dimension in which surface area is increased is not inconsequential. Figure 4 compares the concentration of electrolyte species for catalyst pores having the same surface
area but different proportions of $R$ and $L$. It can be seen that even for the same surface area and $I_{ECSA}$, the difference between the reaction environment within the pores is dramatic.

The construction of the GDE flow-cell system is such that a relatively thin catalyst layer faces a gas-liquid interface on one side and electrolyte flowing in a direction perpendicular to the pore length on the other. As a consequence, the thickness of the catalyst layer ($L$) ends up being the dominant effect and the trend seen in Figure 4 is not very different from the blue curves for $I_{ECSA}=2$ mA/cm$^2$ in Figure 3. Therefore, catalysts with the same surface area but with different catalyst layer thickness can be expected to show very different selectivity for CO$_2$ reduction. Experimentally, identical catalytic materials may then give the appearance of varying catalytic activity when in fact only the orientation may be different.

**Geometric vs ECSA normalized current density**

Figure 5 and S3 demonstrate the difference between comparing the reaction environment within the catalyst pores at a fixed ECSA vs. geometrically normalized current density. $I_{geom}$ is fixed (red dotted curve) such that the $I_{ECSA}$ is 1 mA/cm$^2$ for a pore of length 100 nm. The roughness factor is assumed to be directly proportional to the pore surface area and the $I_{ECSA}$ is adjusted accordingly to keep $I_{ECSA} * f_r$ or $I_{geom}$ constant (see equation
Figure 5: A comparison between median pH and cation concentration within pore derived for constant $I_{geom}$ vs. constant $I_{ECSA}$ of 1 mA/cm$^2$. The annotations on the red dotted curve signify the value of $I_{ECSA}$ corresponding to the respective pore size for the constant $I_{geom}$. The radius of pore ($R$) is 5 nm for all cases.

24). The pH or the cation concentration within the pore does not change significantly when compared at constant $I_{geom}$ unlike at a constant $I_{ECSA}$. However, a comparison of different catalysts at constant $I_{geom}$ is not useful for isolating the influence of the inherent catalytic activity and the reaction environment by not taking into account the active surface area of the catalyst.$^{71-73}$ Collectively, these results communicate the challenges associated with interpreting experimental data commonly reported in the form of geometric current density, and comparing data sets performed under varying ECSA current density.

**Effective diffusion coefficient in catalyst pore**

One of the effects of changing the porous structure of the catalyst is the change in the effective diffusion coefficient of electrolyte species as given by equation (19). For catalyst pores flooded with electrolyte, the ratio of the effective and bulk diffusion coefficient ($D_{eff}^i/D^i$) for a species can range between 0 and 1. Figure S2 in the SI shows how changing this ratio has no considerable effect on the median reaction environment within the pore. Therefore, it can be concluded that unless the medium of species transport within the pore changes, the change in the effective diffusion coefficient of species with changing catalyst structure is
not an important effect. The effective porosity ($\epsilon$), constrictivity ($\delta$) and tortuosity ($\tau$) are however, influential factors as they are directly related to the catalyst structure.

**Boundary conditions and choice of model**

The CL thickness is typically in the order of a few 100 nm in a typical GDE based flow-cell, which is small relative to the thickness of a gas-diffusion layer and the electrolyte diffusion layer. Consequently, the boundary conditions at $S_1$ and $S_3$ for the CL play a hugely important role in determining the reaction conditions as they act as the entry and exit point of all species. Transport and replenishment in these layers is likely more limiting than within the GDE pores. The following sections discuss the influence of the electrolyte flow rate at the electrolyte-electrolyte-interface $S_3$, the gas pressure at the gas-electrolyte interface $S_1$ and the applied potential at the catalyst surface $S_2$ on the environment within the model pore.

**Electrolyte flow rate**

![Figure 6: Effect of changing Reynolds number on the median pH and concentration of charged species in the catalyst pore. Reynolds numbers of 28, 140, 280, 1120 and 1960 corresponds to electrolyte flow velocities ($|v_e|/A_{\text{cross}}$ in equation (14)) of 0.1 m/min, 0.5 m/min, 1 m/min, 4 m/min and 7 m/min, respectively. A pore of 5 nm x 100 nm ($R \times L$) and $I_{\text{ECSA}}=2$ mA/cm$^2$ is used for all data points.](image)


Figure 6 shows the influence of changing the Reynolds number for the electrolyte flow at the electrolyte-electrolyte interface in a direction perpendicular to the pore length (see Figure 1a). The default Reynolds number according to our typically laboratory setup is calculated to be $\sim 28$. This is equivalent to an electrolyte flow velocity of 0.1 m/min or a volumetric flow of 15 ml/min (|v_e|) across a flow channel with cross section of 1.5 cm$^2$ ($A_{cross}$) as per equation (14). The Reynolds number for the electrolyte flow influences the flux of species at the interface $S_3$ according to the equations (12) - (15).

The pH within the catalyst pore reduces dramatically on increasing the Reynolds number as seen in Figure 6a by increasing the flux of OH$^-$ ions out of the pore towards the bulk electrolyte. The red curve for HCO$_3^-$ in Figure 6b follows the pH trend signifying buffer breakdown at low electrolyte flow rates. Although, the CO$_2$ concentration in the pore does not change significantly due to Reynolds number as shown in Figure S4, the concave nature of the curve demonstrates the competition between CO$_2$ solubility based on the ionic concentration within the pore and the outward flux of the CO$_2$ at $S_3$. Experimentally, flow rate of electrolyte has been shown to influence the catalyst selectivity in experimental studies using flow-cells. This is not surprising considering the extent to which electrolyte flow can potentially alter conditions within the CL. Management of pressure drop across the GDE can however, be a non-trivial aspect of the operation of the flow-cell and can possibly limit the use of electrolyte flow rate as a control mechanism for product selectivity.

**Gas pressure**

Gas pressure has also been used as an operational handle to tune product selectivity in flow-cells. A variation in gas-pressure will need adjustment of the liquid pressure in order to maintain the gas-electrolyte interface at $S_1$ such that the capillary pressure of the pores plus the liquid pressure balance the gas pressure. A pressure imbalance can lead to either gas channels entering the CL pores or flooding of the GDL, which will significantly change the nature of mass transport within the CL. We assume that $S_1$ remains stationary after
increasing the gas pressure and that the electrolyte properties remain unchanged.

Figure S5 in the SI shows the influence of increasing pressure at the gas-electrolyte interface \( S_1 \) on the reaction environment within the pore. Increasing the gas pressure from 1 bar to 10 bar leads to a reduction in the pH by \( \sim 0.8 \) units and factor of 10 increase in the median CO\(_2\) concentration. The reduction of pH on increasing gas pressure also results in an increase in CO\(_3^{2-}\) and K\(^+\) as a consequence of the buffer reactions and the electrostatic interactions in the electrolyte. In terms of pH, the effect of increasing the gas pressure by a factor of 10 is very similar to the effect of reducing the electrolyte flow velocity by a factor of 10 at the electrolyte-electrolyte interface (see drop in pH between a Reynolds number of 28 and 280 in Figure 6a). The influence on the CO\(_2\) availability within the pore however, is very different for the two scenarios. Both operational handles of gas pressure and electrolyte flow involve practical challenges regarding management of flooding of the GDL and electrolyte distribution within the CL. The appropriate control mechanism for reaction conditions can be chosen based on whether CO\(_2\) concentration becomes limiting through the CL (for thick layers) and the stability of the gas-electrolyte interface.

**Applied potential**

We compare the output from a reaction diffusion model (model details in the SI) with the GMPNP model to understand the influence of taking applied potential at the catalyst surface \( S_2 \) into account. A reaction-diffusion model does not take electrostatic effects of the system and reaction interface into account, and will thus lead to different steady-state concentrations of species within the GDE pore as compared to the GMPNP model.

For the small pore radius of 5 nm and a small applied potential of -25 mV vs PZC used as a boundary condition for the GMPNP model, the median pH (Figure 7a) and buffer breakdown (Figure S6) with changing pore length does not vary significantly between the two models. This is not surprising, since the effect of the EDL formation is restricted to
Figure 7: Comparing the median concentration of species in the catalyst pore with changing pore length \((L)\) derived using a reaction-diffusion model and a GMPNP model. A pore of 5 nm x 100 nm \((R \times L)\) and \(I_{ECSA}=2\) mA/cm\(^2\) is used for all data points.

\(~1\) nm around the catalyst surface at the small applied potential and is not expected to perturb the median \(H^+\) concentration of the pore drastically. The slightly low pH obtained for GMPNP is owing to the fact that the catalyst surface is negatively charged leading to a build-up of positively charged ions in the EDL.

Comparing the predicted \(CO_3^{2-}\) and \(K^+\) concentrations between the two models, however, a much larger discrepancy is observed. In the reaction diffusion model the ion concentrations are predicted to be much higher than in the case of the GMPNP model (Figures 7c and 7d). The model differences are a result of the applied electric field in the GMPNP model which drives the repulsion of \(CO_3^{2-}\) from the GDE pore, leading to an overall different
balance of charged species versus the reaction-diffusion model. Critically, this variation in-
turn influences the solubility of CO$_2$ in the electrolyte and results in the deviating trends
seen for median CO$_2$ concentration in Figure 7b.

![Common scale](image1)

![GMPNP](image2)

![RD](image3)

Figure 8: A comparison of CO$_2$ concentration along a longitudinal cross-section of a pore
with $R \times L$ of 5 nm x 100 nm and $I_{ECSA}=2$ mA/cm$^2$ for the GMPNP and reaction-diffusion
(RD) model. An applied potential of -25 mV vs PZC for the catalyst surface is used for the
GMPNP model. The gas-liquid interface is the left edge whereas the electrolyte-electrolyte
interface is the right edge with the top and bottom edges being part of the catalyst surface.
(a) shows the output of the GMPNP and RD model on the same scale for comparison. (b)
and (c) show the distribution on separate scales for clarity.

Figure 8 shows the spatial CO$_2$ concentration along a longitudinal cross-section of the
pore. The concentration of CO$_2$ does not vary significantly within the pore for either of the
models as can be seen from Figure 8a. However, making the concentration scales narrower
for each model reveals a very different distribution of CO$_2$, both radially and longitudinally. The concentration profile obtained using the GMPNP model in Figure 8b clearly captures the edge effects due to the presence of the electric field at the catalyst surface as well as ion accumulation in the EDL which are absent in the reaction-diffusion model in Figure 8a. Similar comparisons for other solution species can be found in Figures S7b, S9a, S8b and S10 in the SI.

Increasing the radius of the pore is expected to diminish the influence of the EDL on the median concentration predicted by the GMPNP. On the other hand, a higher applied potential should further exaggerate the differences in the prediction from the GMPNP vs. the reaction-diffusion model. Using the reaction-diffusion model to derive trends for median reaction conditions in the pore volume can be a reasonable choice, especially when studying pores with large radii and lengths. However, if it is desired to study the edge effects in these systems such as the environment in the vicinity of the interfaces, the reaction-diffusion model can be grossly insufficient owing to the missing electrostatic effects.

Lastly, it is worth noting that the curvature of pores with $\geq$ 5 nm radius is expected to be large enough for the EDL to behave similar to a flat plate and 1D simulations such as presented in reference 43 can instead be used to specifically study the EDL properties.\textsuperscript{76} The arrangement of ions within pores with radii similar in length scale to the EDL can no longer be accurately predicted using continuum models and requires molecular level treatment.\textsuperscript{77–79} Pores with high curvature (small radii) can make the limitations of the current GMPNP model even more pronounced, especially regarding the treatment of solvent water molecules and their relative interaction with the hydrophilic catalyst surface vs. the ionic species, van der Waals forces and Coulombic interaction between charged species.\textsuperscript{80} It is not expected for pores below 5 nm radius to have a significant population in the CL and therefore can be safely ignored for building models for the CL.\textsuperscript{22,58}
Conclusions

An effective flooded cylindrical catalyst pore was used to study the influence of changing pore geometry and boundary conditions on the reaction environment during eCO$_2$R in a GDE-based flow cell setup. The length of the catalytic pore was found to be an important parameter, determining the pH, buffer breakdown and concentration of ionic species in the pore. We find that pores with the same surface area but different lengths can have very different reaction environments. The thickness of the deposited catalyst layer on top of the GDL is therefore expected to be an important design handle for optimizing performance. The flux of species across the gas-electrolyte interface at the MPL/CL boundary as well as across the electrolyte-electrolyte interface also play a significant role in determining the reaction conditions within the CL. The transport properties and operating conditions for the gas flow, the gas composition and pressure, and the electrolyte flow rate and flow-channel geometry, are therefore expected to have a major influence on the resultant catalyst selectivity and activity. A comparison of the GMPNP model with the reaction-diffusion model shows that the applied potential is an important parameter for ionic concentration within the pore, which in turn influences the CO$_2$ solubility in the electrolyte. Reaction-diffusion model can be sufficient for studying median concentration of species within the catalyst layer for pores with large radii and length since the influence of the relatively thin electrical double layer (EDL) diminishes with the increasing pore volume. However, considering the electrostatic effect of the applied potential becomes essential if studying edge effects and the environment in the vicinity of the catalyst surface is the aim.

Management of pressure drop across the various system components to maintain the desired gas-electrolyte interfaces for catalysis can be very challenging for practical operation of flow-cell systems. There is a need to better understand the wetting properties of the catalyst layer and the parameters influencing flooding, film thickness and formation of vapor channels in this layer. Fluid dynamics is therefore an important aspect of flow-cell
systems and should be coupled with the PNP equations to model the transport and possible two-phase flow within the CL. Lastly, a major challenge in modeling heterogeneous porous catalytic systems lies in the upscaling of microscopic models such as the one reported here to the macroscopic level. Developing upscaling frameworks to accurately model the influential aspects of the mass transport will be an important step to study the performance of GDE-based eCO₂R systems. The presence of 2-phase interfaces and electrolyte flow at the boundaries of a relatively thin, charged and nanostructured catalyst layer, make mass transport central to the performance of flow-cell setups for eCO₂R. The sensitivity of the catalysis to structural and operational parameters for such systems will be significantly higher than the traditionally studied H-cells. The field should therefore move towards benchmarking of system performance against these parameters to improve reproducibility and shorten the development cycle towards an industrial scale system.

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Supporting Information Available

Supporting modeling details, parameter values and simulation results available.

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Supporting Information:
Mass transport in catalytic pores of GDE-based CO₂ electroreduction systems

Divya Bohra,† Jehanzeb H. Chaudhry,† Thomas Burdyny,† Evgeny A. Pidko,¶
and Wilson A. Smith*,†,§,∥

†Materials for Energy Conversion and Storage (MECS), Department of Chemical Engineering, Delft University of Technology, Delft, The Netherlands
‡Department of Mathematics and Statistics, University of New Mexico, Albuquerque, USA
¶Inorganic Systems Engineering (ISE), Department of Chemical Engineering, Delft University of Technology, Delft, The Netherlands
§Department of Chemical and Biological Engineering, University of Colorado Boulder, Boulder, USA
∥National Renewable Energy Lab, Golden, USA

E-mail: wilson.smith@colorado.edu
Model details

Calculating bulk concentrations

We assume Henry’s law to be valid for CO$_2$ gas and calculate its concentration in water using equation (1). We assume the fugacity of CO$_2$ to be 1 bar.

$$C_{CO_2,aq}^0 = K_H^0 C_{CO_2,g}$$  \hspace{1cm} (1)

where $K_H^0$ is Henry’s constant and is given as a function of temperature T by equation (2).$^{S1}$ The temperature is assumed to be 298.15 K for our calculations.

$$\ln K_H^0 = 93.4517 \ast \left( \frac{100}{T} \right) - 60.2409 + 23.3585 \ast \ln \left( \frac{T}{100} \right)$$  \hspace{1cm} (2)

The saturated concentration of CO$_2$ in an electrolyte ($C_{CO_2,aq}$) with 0.1 M KHCO$_3$ is then given by equation (3).$^{S2}$

$$\log \left( \frac{C_{CO_2,aq}^0}{C_{CO_2,aq}} \right) = K_S C_S$$  \hspace{1cm} (3)

where $C_S$ is the molar concentration of the electrolyte (0.1) and $K_S$ is the Sechenov’s constant and can be estimated using parameters $h_i$ for species $i$. Values of $h$ for all species can be found in the Parameters section.

$$K_S = \sum (h_{CO_2} + h_{ion})$$  \hspace{1cm} (4)

$$h_{CO_2} = h_{CO_2}^0 + h_{CO_2}^T (T - 298.15)$$  \hspace{1cm} (5)

In order to calculate the concentration of solution species in the bulk electrolyte, the Sechenov equation (3) is used to estimate the saturated concentration of CO$_2$ in a 0.1 M KHCO$_3$ electrolyte. The estimated CO$_2$ concentration is then used to solve the rate equations.
(9) to (13) (corresponding to equations (6), (7) and (8)) till steady state is reached.

\[
\begin{align*}
\text{H}_2\text{O} & \xrightarrow{k_{w1}} \text{H}^+ + \text{OH}^- \\
\text{HCO}_3^- + \text{OH}^- & \xrightarrow{k_{a1}} \text{CO}_3^{2-} + \text{H}_2\text{O} \\
\text{CO}_2 + \text{OH}^- & \xrightarrow{k_{b1}} \text{HCO}_3^- \\
R_{H^+} &= \frac{\partial C_{H^+}}{\partial t} = -k_{w2} C_{H^+} C_{OH^-} + k_{w1} \\
R_{OH^-} &= \frac{\partial C_{OH^-}}{\partial t} = -k_{w2} C_{H^+} C_{OH^-} - k_{a1} C_{OH^-} C_{HCO_3^-} \\
- k_{b1} C_{CO_2} C_{OH^-} + k_{w1} + k_a C_{CO_3^{2-}} + k_{b2} C_{HCO_3^-} \\
R_{HCO_3^-} &= \frac{\partial C_{HCO_3^-}}{\partial t} = \\
- k_{a1} C_{OH^-} C_{HCO_3^-} - k_{b2} C_{HCO_3^-} + k_{a2} C_{CO_3^{2-}} + k_{b1} C_{CO_2} C_{OH^-} \\
R_{CO_3^{2-}} &= \frac{\partial C_{CO_3^{2-}}}{\partial t} = - k_{a2} C_{CO_3^{2-}} + k_{a1} C_{OH^-} C_{HCO_3^-} \\
R_{CO_2} &= \frac{\partial C_{CO_2}}{\partial t} = - k_{b1} C_{CO_2} C_{OH^-} + k_{b2} C_{HCO_3^-} \\
\end{align*}
\]

The resulting bulk species concentrations for a 0.1 M \text{KHCO}_3 electrolyte saturated with \text{CO}_2 at 1 bar and room temperature are (in mM): $C_{CO_2}^0 = 34.061$, $C_{CO_3^{2-}}^0 = 0.039$, $C_{H^+}^0 = 0.00014$, $C_{HCO_3^-}^0 = 99.920$, $C_{K^+}^0 = 100.0$, $C_{OH^-}^0 = 7.1e-05$, pH = 6.853.

**Scaling the 3D GMPNP equations**

Below are the scaled MPNP and Poisson equations corresponding to equations (17), (18) and (20) in the main text.
\[
\frac{\partial \tilde{C}_i}{\partial \Gamma} = \tilde{\nabla} \cdot \left( \tilde{\nabla} \tilde{C}_i + \tilde{C}_i z_i \tilde{\nabla} \Phi + \tilde{C}_i \left( \frac{\sum^{n}_{i=1} v_i \tilde{\nabla} \tilde{C}_i}{1 - \sum^{n}_{i=1} v_i \tilde{C}_i} \right) \right) + \sum_{j} \vartheta_j R_{ij} \tag{14}
\]

\[
\tilde{\nabla} \cdot \left( \varepsilon_r \tilde{\nabla} \Phi \right) = - \sum_{i=1}^{n} q_i z_i \tilde{C}_i \tag{15}
\]

\[
\Lambda = \frac{R}{L} \tilde{x} = \frac{x}{L}, \tilde{y} = \frac{y}{L}, \tilde{z} = \frac{z}{L}, \Gamma = \frac{t D_i^{\text{eff}}}{L^2}, \tilde{C}_i = \frac{C_i}{C_0^i}, \Phi = \frac{\phi F}{R_G T}, \vartheta_i = \frac{a_i^3 N_A C_0^i}{\varepsilon_0 R_G T}, q_i = \frac{(FL)^2 C_0^i}{\varepsilon_0 R_G T} \]

\[
\tilde{\nabla} u = \frac{\partial u}{\partial \tilde{x}} \tilde{e}_x + \frac{\partial u}{\partial \tilde{y}} \tilde{e}_y + \frac{\partial u}{\partial \tilde{z}} \tilde{e}_z \tag{16}
\]

\[
\tilde{\nabla}^2 u = \frac{\partial^2 u}{\partial \tilde{x}^2} \tilde{e}_x + \frac{\partial^2 u}{\partial \tilde{y}^2} \tilde{e}_y + \frac{\partial^2 u}{\partial \tilde{z}^2} \tilde{e}_z \tag{17}
\]

where \( L \) is the length and \( R \) is the radius of the cylindrical pore with OHP as the outer cylindrical boundary and \( C_0^i \) is the bulk concentration of species \( i \). Scaling all length dimensions with the same constant \( (L) \) leads to a simpler computational implementation of the weak form in FEniCS.

Consequently, the equations (14) and (15) need to be solved simultaneously with the appropriate initial and boundary conditions to obtain the species concentration and potential profiles at steady state.

**Galerkin form in 3D**

In order to solve the GMPNP equations using FEniCS, we need to derive the Galerkin (or the weak form) of the non-linear partial differential equations (14) and (15). We use an implicit Euler time discretization with the volume element \( dV \) defined as \( d\tilde{x}d\tilde{y}d\tilde{z} \) and
gradient defined for the scaled cartesian coordinates as given in equation (16). \( p_i \) and \( s \) are the test functions for \( \tilde{C}_i \) and \( \Phi \) in the Galerkin form, respectively. The surface integral term becomes zero in case of a Dirichlet boundary condition or is defined using the surface fluxes as a Neumann boundary condition. In equation (19), \( \mathbf{n} \) is the outward normal direction to the respective surface.

\[
\int_{V} \left( \frac{\tilde{C}_{i}^{n+1} - \tilde{C}_{i}^{n}}{\Delta t} \right) p_i dV \\
+ \int_{V} \left[ \tilde{\nabla} \tilde{C}_i \tilde{\nabla} p_i + z_i \tilde{C}_i \tilde{\nabla} \Phi \tilde{\nabla} p_i + \tilde{C}_i \left( \frac{\sum_{i=1}^{n} u_i \tilde{\nabla} \tilde{C}_i}{1 - \sum_{i=1}^{n} u_i \tilde{C}_i} \right) \tilde{\nabla} p_i - p_i \vartheta_i \sum_{j} R_{ij} \right] dV
\]

\[
+ \int_{S_1} \mathbf{J}^{S_1} \cdot \sigma_i dS_1 + \int_{S_2} \mathbf{J}^{S_2} \cdot \sigma_i dS_2 + \int_{S_3} \mathbf{J}^{S_3} \cdot \sigma_i dS_3 = 0 \quad (18)
\]

\[
\int_{V} \left[ s \sum_{i=1}^{n} q_i z_i \tilde{C}_i - \varepsilon_r \tilde{\nabla} \Phi \tilde{\nabla} s \right] dV \\
+ \int_{S_1} \frac{\partial \Phi}{\partial n} \varepsilon_r s dS_1 + \int_{S_2} \frac{\partial \Phi}{\partial n} \varepsilon_r s dS_2 + \int_{S_3} \frac{\partial \Phi}{\partial n} \varepsilon_r s dS_3 = 0 \quad (19)
\]

**Reaction-diffusion model**

In the reaction-diffusion model, the flux term in the mass balance equation only contains the diffusion mass transport term and excludes the migration and volume correction terms as given below.

\[
\frac{\partial C_i}{\partial t} = -\nabla \cdot \mathbf{J}_i + \sum_{p} R_i \quad (20)
\]

\[
\mathbf{J}_i = -D_i \nabla C_i \quad (21)
\]
Parameters

Rate-constants:

| Constant | Value     | Units               | Reference |
|----------|-----------|---------------------|-----------|
| kw1      | 2.4e-2    | mol·m⁻³·s⁻¹         | S3–S5     |
| kw2      | 2.4e+6    | mol⁻¹·m³·s⁻¹        | S3–S5     |
| ka1      | 6.0e+6    | mol⁻¹·m³·s⁻¹        | S6        |
| ka2      | 1.07e+6   | s⁻¹                 | S6        |
| kb1      | 2.23      | mol⁻¹·m³·s⁻¹        | S6        |
| kb2      | 5.23e-5   | s⁻¹                 | S6        |

Diffusion-coefficients in $m²·s^{-1}$:

| Constant | Value     | Reference |
|----------|-----------|-----------|
| $D_{H^+}$ | 9.311e-9  | S3,S4     |
| $D_{OH^-}$ | 5.273e-9  | S3,S4     |
| $D_{CO}_2$ | 1.91e-9   | S3,S4     |
| $D_{CO}$   | 2.03e-9   | S7        |
| $D_{H_2}$  | 4.5e-9    | S7        |
| $D_{HCO_3^-}$ | 1.185e-9 | S3,S4     |
| $D_{CO_3^-}$ | 0.923e-9  | S3,S4     |
| $D_{K^+}$  | 1.957e-9  | S8        |
| $D_{Na^+}$ | 1.334e-9  | S8        |
| $D_{Li^+}$ | 1.029e-9  | S8        |
| $D_{Cs^+}$ | 2.06e-9   | S8        |

1* The solvated size of HCO$_3^-$ is assumed to be similar to CO$_3^{2-}$ due to unavailability of a reliable value in literature. ** The solvated size of CO$_2$, CO and H$_2$ are assumed based on bond distances without solvation.
Solvation sizes in \( m \)^{39}

| Constant | Value       |
|----------|-------------|
| \( a_{H^+} \) | 0.56e-9     |
| \( a_{OH^-} \) | 0.6e-9      |
| \( a_{\text{CO}_2}^{**} \) | 0.23e-9     |
| \( a_{\text{CO}}^{**} \) | 0.113e-9    |
| \( a_{H_2}^{**} \) | 0.074e-9    |
| \( a_{\text{HCO}_3}^* \) | 0.8e-9      |
| \( a_{\text{CO}_3}^- \) | 0.788e-9    |
| \( a_{K^+} \) | 0.662e-9    |
| \( a_{Na^+} \) | 0.716e-9    |
| \( a_{Li^+} \) | 0.764e-9    |
| \( a_{Cs^+} \) | 0.658e-9    |

Parameters used to estimate Sechenov’s constant in \( m^3 \cdot kmol^{-1} \)^{32}

| Constant | Value |
|----------|-------|
| \( h_{K^+} \) | 0.0922 |
| \( h_{OH^-} \) | 0.0839 |
| \( h_{\text{HCO}_3}^- \) | 0.0967 |
| \( h_{\text{CO}_3}^- \) | 0.1423 |
| \( h_{\text{CO}_2}^0 \) | -0.0172 |
| \( h_{\text{CO}_2}^T \) | -0.000338 |
Hydration numbers for cations:  
\[ S_{10},S_{11} \]

| Constant | Value |
|----------|-------|
| \( w_{K^+} \) | 4     |
| \( w_{Li^+} \) | 5     |
| \( w_{Na^+} \) | 5     |
| \( w_{Cs^+} \) | 3     |
| \( w_{H^+} \) | 10    |

Henry’s constants for gases in water in \( mol \cdot kg^{-1} \cdot bar^{-1} \):  
\[ S_{12} \]

| Constant | Value |
|----------|-------|
| \( H_{CO_2} \) | 0.034 |
| \( H_{CO} \) | 0.00095 |
| \( H_{H_2} \) | 0.00078 |

Potential at the point of zero charge in V vs SHE at pH=7:  
\[ S_{13} \]

| Surface | Value |
|---------|-------|
| Ag-pc   | -0.70 |
| Ag(111) | -0.450 |
| Ag(110) | -0.735 |
| Ag(100) | -0.616 |

Other constants

| Constant | Value | Units       |
|----------|-------|-------------|
| \( \rho_e \) | 997   | kg·m⁻³     |
| \( \mu_e \) | 0.89e⁻³ | kg·m⁻¹·s⁻¹ |
| \( L_c \) | 1.5e⁻² | m          |
| \( v_e \) | 0.25e⁻⁶ | m³·s⁻¹    |
| \( A_{cross} \) | 1.5e⁻⁴ | m²        |
| \( L_{cross} \) | 1.0e⁻² | m         |
Supplementary Results: 3D GMPNP model

Figure S1: Influence of changing length ($L$) of effective catalyst pore on median carbonate ion concentration within the pore. The radius ($R$) of all pores is 5 nm.

Figure S2: Influence of changing the ratio of effective to bulk diffusion coefficient of electrolyte species on their median concentration in pore. A pore of 5 nm x 100 nm ($R \times L$) and $I_{ECSA}=2$ mA/cm$^2$ is used for all data points.
Figure S3: A comparison between median species concentrations within pore derived for constant $I_{geom}$ vs. constant $I_{ECSA}$. The annotations on the red dotted curve signify the value of $I_{ECSA}$ corresponding to the respective pore size for the constant $I_{geom}$. The radius ($R$) of all pores is 5 nm.

Figure S4: Effect of changing Reynolds number on CO$_2$ concentration in the catalyst pore. A pore of 5 nm x 100 nm ($R \times L$) and $I_{ECSA}$=2 mA/cm$^2$ is used for all data points.

Figure S5: Influence of changing the total gas pressure at the gas-electrolyte interface on the median concentration of electrolyte species in the pore. A pore of 5 nm x 100 nm ($R \times L$) and $I_{ECSA}$=2 mA/cm$^2$ is used for all data points.
Figure S6: Comparing the median concentration of $\text{HCO}_3^-$ in the catalyst pore with changing pore length ($L$) derived using a reaction-diffusion model and a GMPNP model. A pore of 5 nm x 100 nm ($R \times L$) and $I_{ECSA}=2 \text{ mA/cm}^2$ is used for all data points.
Figure S7: A comparison of pH along a longitudinal cross-section of a pore with $R \times L$ of 5 nm x 100 nm and $I_{ECSA}=2$ mA/cm$^2$ for the GMPNP and reaction-diffusion (RD) model. An applied potential of -25 mV vs PZC for the catalyst surface is used for the GMPNP model. The gas-liquid interface is the left edge whereas the electrolyte-electrolyte interface is the right edge with the top and bottom edges being part of the catalyst surface. (a) shows the output of the GMPNP and RD model on the same scale for comparison. (b) and (c) show the distribution on separate scales for clarity.
Figure S8: A comparison of CO$_3^{2-}$ concentration along a longitudinal cross-section of a pore with $R \times L$ of 5 nm x 100 nm and $I_{ECSA}=2$ mA/cm$^2$ for the GMPNP and reaction-diffusion (RD) model. An applied potential of -25 mV vs PZC for the catalyst surface is used for the GMPNP model. The gas-liquid interface is the left edge whereas the electrolyte-electrolyte interface is the right edge with the top and bottom edges being part of the catalyst surface. (a) shows the output of the GMPNP and RD model on the same scale for comparison. (b) and (c) show the distribution on separate scales for clarity.
Figure S9: A comparison of \( \text{OH}^- \) concentration along a longitudinal cross-section of a pore with \( R \times L \) of 5 nm x 100 nm and \( I_{ECSA}=2 \text{ mA/cm}^2 \) for the GMPNP and reaction-diffusion (RD) model. An applied potential of -25 mV vs PZC for the catalyst surface is used for the GMPNP model. The gas-liquid interface is the left edge whereas the electrolyte-electrolyte interface is the right edge with the top and bottom edges being part of the catalyst surface. (a) shows the output of the GMPNP and RD model on the same scale for comparison. (b) shows the distribution on a separate scales for the RD model for clarity.
Figure S10: A comparison of dissolved CO (a) and H\(_2\) (b) concentrations along a longitudinal cross-section of a pore with \(R \times L = 5 \text{ nm} \times 100 \text{ nm}\) and \(I_{ECSA} = 2 \text{ mA/cm}^2\) for the GMPNP and reaction-diffusion (RD) model. An applied potential of -25 mV vs PZC for the catalyst surface is used for the GMPNP model. The gas-liquid interface is the left edge whereas the electrolyte-electrolyte interface is the right edge with the top and bottom edges being part of the catalyst surface.
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