Limits on contact interactions and leptoquarks at HERA

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I. INTRODUCTION

The H1 and ZEUS collaborations measured inclusive $e^\pm p$ scattering cross sections at HERA from 1994 to 2000 (HERA I) and from 2002 to 2007 (HERA II), collecting a total integrated luminosity of approximately 1 fb$^{-1}$. All the inclusive data sets were combined [1] to create one consistent set of neutral current (NC) and charged current (CC) cross-section measurements for $e^\pm p$ scattering with unpolarized beams. These cross sections were used as input to a QCD analysis within the Dokshitzer-Gribov-Lipatov-Altarelli-Parisi [2–6] formalism of the Standard Model (SM), resulting in parton distribution function (PDF) parametrizations of the proton denoted as HERAPDF2.0 [1]. Precise knowledge of the parton densities inside the proton is crucial, in particular, for the full exploitation of the physics potential of the LHC.

HERA measurements of deep inelastic $e^\pm p$ scattering (DIS) cross sections at the highest values of negative four-momentum-transfer squared, $Q^2$, can be sensitive to beyond the Standard Model (BSM) contributions even at scales far beyond the center-of-mass energy of 320 GeV. For many “new physics” scenarios, cross sections can be affected by new kinds of interactions in which virtual BSM particles are exchanged. As the HERA center-of-mass energy is assumed to be far below the scale of the new physics, all such BSM interactions can be approximated as contact interactions (CIs).

In the absence of direct observation of BSM physics at HERA, the ZEUS collaboration has used the HERA combined measurement of inclusive cross sections [1] to set limits on possible deviations from the SM due to a finite quark radius [7]. If BSM physics effects existed in the HERA data, the current PDF sets would have been biased by partially or totally absorbing unrecognized BSM contributions. A new approach was therefore used to minimize this bias, based on simultaneous fits of the PDFs and the contributions of “new physics” processes. It was assumed, as usual, that the use of SM Monte Carlo simulations in the original extraction of the cross sections did not introduce a significant bias. The new procedure [7] introduced to set limits on the quark radius has also been extended to other...
“new physics” scenarios. BSM contributions were added to the fit to HERA data to investigate whether this results in an improvement of the description of the data. Previous CI searches [8–10] used only a subset of the HERA data used here.

II. MODELS FOR NEW PHYSICS

Four-fermion CIs represent an effective theory which describes low-energy effects due to physics at much higher energy scales. Contact-interaction models can describe the effects of heavy leptoquarks, additional heavy weak bosons and electron or quark compositeness [11]. The CI approach is not renormalizable and is only valid in the low-energy limit, far below the mass scale of the new physics. For HERA data collected at center-of-mass energy of 320 GeV this approach should be applicable for new physics mass scales of about 1 TeV or above. Vector CI currents considered here are represented by additional terms in the SM Lagrangian:

\[ \mathcal{L}_{CI} = \sum_{i,j=L,R} \sum_{q=u,d,s} \left( \eta_{ij}^{eq} \overline{q}_i \gamma^\mu e_j \right) \left( \overline{q}_j \gamma_\mu q_i \right), \]

where the sum runs over electron and quark chiralities and quark flavors. The couplings \( \eta_{ij}^{eq} \) describe the chiral and flavor structure of CIs.

The CI contributions to the electron-quark scattering amplitude do not depend on the \( Q^2 \) scale of the process. Thus, the CI contributions to the DIS cross sections are expected to be largest, relative to the SM contribution, at the highest \( Q^2 \) values [12]. However, the exact shape of the expected deviations from the SM predictions depends on the assumed flavor and chiral structure of the CI couplings. Depending on the coupling structure, different contributions are also expected for electron-proton and positron-proton scattering.

A. Contact interactions

For this study, the CI scenarios were defined assuming that all quarks have the same CI couplings:

\[ \eta_{ij}^{eq} = \eta_{ij}^{ed} = \eta_{ij}^{es} = \eta_{ij}^{ec} = \eta_{ij}^{ek}, \]

leading to four independent couplings, \( \eta_{ij}^{eq} \), with \( i, j = L, R \). Owing to the impracticality of setting limits in a four-dimensional parameter space, a set of one-parameter scenarios was analyzed. Each scenario is defined by a set of four coefficients, \( \epsilon_{ij} \), each of which may take the values \( \pm 1 \) or zero, see Table I, and by the coupling strength \( \eta \) or compositeness scale \( \Lambda \). The couplings are given by the formula

\[ \eta_{ij}^{eq} = \eta \epsilon_{ij} = \pm \frac{4\pi}{\Lambda^2} \epsilon_{ij}. \]

Four parity-violating scenarios were selected for this study. They are listed in the upper part of Table I. In addition, nine scenarios conserving parity were chosen, shown in the lower part of Table I, for which the bounds resulting from atomic-parity violation measurements are not relevant. These models were first introduced in a previous ZEUS publication [13]. Note that the coupling strength \( \eta \) can be both positive and negative, and the two cases are distinct because of the interference with the SM amplitudes [11,12]. Only in the case of the VA model (see Table I) is the contribution of the interference term negligible, so that the model predictions are mainly sensitive to \( \eta^2 \). When setting limits for BSM contributions, scenarios with positive and negative \( \eta \) values were considered separately.

B. Heavy leptoquarks

Leptoquarks (LQs) appear in certain extensions of the SM that connect leptons and quarks; they carry both lepton and baryon numbers and have spin 0 (in case of scalar LQs) or 1 (vector LQs). According to the general classification proposed by Buchmüller, Rückl and Wyler [14], there are 14 possible LQ types (isospin singlets or multiplets): seven scalar and seven vector.1 In the limit of heavy LQs (for masses much higher than the HERA center-of-mass energy, \( M_{LQ} \gg \sqrt{s} \)), the effect of \( s \)- and \( t \)-channel LQ exchange is equivalent to a vector-type \( eeqq \) contact interaction.2

The effective LQ coupling, \( \eta_{LQ} \), is given by the square of the ratio of the leptoquark Yukawa coupling, \( \lambda_{LQ} \), to the leptoquark mass, \( M_{LQ} \):

\[ \eta_{LQ} = \left( \frac{\lambda_{LQ}}{M_{LQ}} \right)^2. \]

The CI couplings of the Lagrangian [Eq. (1)], \( \eta_{ij}^{eq} \), can be then written as

\[ \eta_{ij}^{eq} = a_{ij}^{eq} \cdot \eta_{LQ} = a_{ij}^{eq} \left( \frac{\lambda_{LQ}}{M_{LQ}} \right)^2, \]

where the coefficients \( a_{ij}^{eq} \) depend on the LQ species [17] and are twice as large for vector as for scalar leptoquarks. By definition, the values of \( \eta_{LQ} \) are positive.3 In the analysis presented in this paper, leptoquark couplings are assumed to be family diagonal and only the first-generation LQs are considered, \( q = u, d \). Mass degeneration is assumed for

1Leptoquark states are named according to the so-called Aachen notation [15].

2For the invariant mass range accessible at HERA, with \( \sqrt{s} \approx 320 \text{ GeV} \), the heavy LQ approximation is already applicable for \( M_{LQ} > 400 \text{ GeV} \) [16]. This condition is fulfilled for all scenarios considered here unless \( \lambda_{LQ} \ll 1 \).

3Note that five scalar and five vector LQ models correspond to the same coupling structure but with the opposite coupling sign for scalar and vector scenarios.
TABLE I. Relations between couplings \([\epsilon_{LL}, \epsilon_{LR}, \epsilon_{RL}, \epsilon_{RR}]\) for the considered compositeness models and the CI coupling values, \(\eta^{\text{Data}}\), determined from the simultaneous QCD + CI fit to the HERA inclusive data; \(\delta_{\exp}, \delta_{\text{mod}}\) and \(\delta_{\text{tot}}\) represent the experimental, modeling and total uncertainties, respectively. Also shown is the change of the \(\chi^2\) value relative to the fit performed without the CI contribution, \(\Delta\chi^2 = \chi^2_{\text{SM+CI}} - \chi^2_{\text{SM}}\). For the VA model, two minima in the \(\chi^2\) distribution were considered, separately for negative and for positive coupling values (see text for details).

| Coupling structure | Coupling fits results (TeV^{-2}) |
|--------------------|----------------------------------|
| Model              | \(\epsilon_{LL}, \epsilon_{LR}, \epsilon_{RL}, \epsilon_{RR}\) | \(\eta^{\text{Data}}\) | \(\delta_{\exp}\) | \(\delta_{\text{mod}}\) | \(\delta_{\text{tot}}\) | \(\Delta\chi^2\) |
| LL                 | \([+1, 0, 0, 0]\)               | 0.305                 | 0.206         | +0.017       | +0.207       | -2.06    |
| RR                 | \([0, 0, 0, +1]\)               | 0.338                 | 0.210         | +0.019       | +0.210       | -2.30    |
| LR                 | \([0, +1, 0, 0]\)               | -0.084                | 0.247         | -0.060       | -0.254       | -0.12    |
| RL                 | \([0, 0, +1, 0]\)               | -0.040                | 0.241         | +0.198       | +0.312       | -0.03    |
| VV                 | \([+1, +1, +1, +1]\)           | 0.041                 | 0.061         | +0.004       | +0.066       | -0.45    |
| AA                 | \([+1, +1, -1, +1]\)           | 0.326                 | 0.161         | +0.250       | +0.297       | -4.67    |
| VA                 | \([+1, -1, +1, -1]\)           | -0.594                | 0.225         | -0.120       | -0.255       | -1.21    |
| X1                 | \([+1, -1, 0, 0]\)             | 0.682                 | 0.267         | +0.339       | +0.432       | -5.52    |
| X2                 | \([+1, 0, +1, 0]\)             | 0.089                 | 0.121         | +0.046       | +0.129       | -0.52    |
| X3                 | \([+1, 0, 0, +1]\)             | 0.158                 | 0.108         | +0.009       | +0.109       | -2.09    |
| X4                 | \([0, +1, +1, 0]\)             | -0.029                | 0.116         | +0.098       | +0.151       | -0.06    |
| X5                 | \([0, +1, 0, +1]\)             | 0.079                 | 0.123         | +0.052       | +0.133       | -0.41    |
| X6                 | \([0, 0, +1, -1]\)             | -0.786                | 0.274         | +0.192       | +0.334       | -6.01    |

TABLE II. Coefficients \(a_{ij}^{\text{QG}}\) defining the effective LQ couplings in the CI limit, \(M_{LQ} \gg \sqrt{s}\), and the coupling values, \(\eta^{\text{Data}}_{\text{LQ}}\), determined from the simultaneous QCD + CI fit to the HERA inclusive data, for different models of scalar (upper part of the table) and vector (lower part) LQs; \(\delta_{\exp}, \delta_{\text{mod}}\) and \(\delta_{\text{tot}}\) represent the experimental, modeling and total uncertainties, respectively. Also shown is the change of the \(\chi^2\) value relative to the fit performed without the LQ contribution, \(\Delta\chi^2 = \chi^2_{\text{SM+LQ}} - \chi^2_{\text{SM}}\).

| Model | Coupling structure | \(\eta^{\text{Data}}_{\text{LQ}}\) | \(\delta_{\exp}\) | \(\delta_{\text{mod}}\) | \(\delta_{\text{tot}}\) | \(\Delta\chi^2\) |
|-------|--------------------|----------------------------------|------------------|------------------|------------------|------------------|
| \(S_0\) | \(a_{LL}^{\text{QG}} = +1\) | -0.258              | 0.196           | +0.034          | +0.199          | -1.56            |
| \(S_0\) | \(a_{RR}^{\text{QG}} = +1\) | 0.533              | 0.331           | +0.034          | +0.332          | -2.53            |
| \(S_0\) | \(a_{RL}^{\text{QG}} = +1\) | -2.561             | 1.115           | +0.323          | +1.161          | -3.98            |
| \(S_1/2\) | \(a_{LL}^{\text{QG}} = +1\) | 0.054              | 0.341           | +0.075          | +0.349          | -0.02            |
| \(S_1/2\) | \(a_{RR}^{\text{QG}} = +1\) | 0.112              | 0.491           | +0.118          | +0.505          | -0.05            |
| \(S_1/2\) | \(a_{RL}^{\text{QG}} = -1\) | 0.464              | 1.371           | +0.295          | +1.654          | -0.10            |
| \(S_1/2\) | \(a_{LL}^{\text{QG}} = +1\) | 0.974              | 0.203           | +0.043          | +0.207          | -11.10           |
| \(V_0\) | \(a_{LL}^{\text{QG}} = -1\) | -0.325             | 0.116           | +0.030          | +0.120          | -6.17            |
| \(V_0\) | \(a_{RR}^{\text{QG}} = -1\) | 1.280              | 0.558           | +0.111          | +0.568          | -3.98            |
| \(V_0\) | \(a_{RL}^{\text{QG}} = -1\) | -0.267             | 0.165           | +0.030          | +0.166          | -2.53            |
| \(V_1/2\) | \(a_{LL}^{\text{QG}} = +1\) | -0.232             | 0.685           | +0.132          | +0.698          | -0.10            |
| \(V_1/2\) | \(a_{RR}^{\text{QG}} = +1\) | -0.056             | 0.246           | +0.206          | +0.320          | -0.05            |
| \(V_1/2\) | \(a_{RL}^{\text{QG}} = +1\) | -0.027             | 0.171           | +0.139          | +0.290          | -0.02            |
| \(V_1\) | \(a_{LL}^{\text{QG}} = -1\) | 0.029              | 0.077           | +0.015          | +0.079          | -0.14            |
leptoquark states within isospin doublets and triplets. Contrary to the considered CI scenarios, the LQ coupling structure is different for $u$ and $d$ quarks, resulting in different shapes of the expected cross section deviations. The coupling structure for different leptoquark species is shown in Table II.

**III. EXTENDED FIT TO THE INCLUSIVE HERA DATA**

**A. QCD+CI fit procedure**

The analysis is based on a comparison of the measured inclusive cross sections with the model predictions. The effects of each CI scenario are taken into account by scaling the NLO QCD predictions at given values of $x$ and $Q^2$, corresponding to the inclusive cross section measurements [1], with the cross section ratio

$$R_{CI} = \frac{\sigma_{2, SM+CI}}{\sigma_{2, SM}}$$

(2)
calculated in leading order in electroweak and CI couplings.

The QCD analysis presented in this paper follows the approach adopted for the determination of HERAPDF2.0 [1]. This analysis is extended to take into account the possible BSM contributions to the expected cross section values, as described previously [7]. The PDFs of the proton are described at a starting scale of 1.9 GeV$^2$ in terms of 14 parameters. These parameters, denoted $p^i_k$ in the following (or $p$ for the set of parameters), together with the possible contribution of BSM phenomena (described by the CI coupling $\eta$) were fitted to the data using a $\chi^2$ method, with the $\chi^2$ formula given by

$$\chi^2(p, s, \eta) = \sum_i \frac{[m^i + \sum_j \gamma_j^i m^j s_j - \mu^0_j]^2}{(\delta_{i, \text{stat}} + \delta_{i, \text{uncor}})(\mu^0_j)^2} + \sum_j s_j^2.$$  
(3)

Here, $\mu^0_j$ and $m^i$ are, respectively, the measured cross section values and the SM + CI cross section predictions at the point $i$. The quantities $\gamma_j^i$, $\delta_{i, \text{stat}}$ and $\delta_{i, \text{uncor}}$ are, respectively, the relative correlated systematic, the relative statistical and the relative uncorrelated systematic uncertainties on the input data. The components $s_j$ of the vector $s$ are the correlated systematic shifts of the cross sections (given in units of the respective correlated systematic uncertainties), which were fitted to the data together with PDF parameter set $p$ and the CI coupling $\eta$. The summations extend over all data points $i$ and all correlated systematic uncertainties $j$.

All fits presented here were performed within the xFitter framework [18] modified to include CI contributions. The $\chi^2$ formula was different with respect to that used for the HERAPDF2.0 study [1] to reflect the fact that fixed Gaussian uncertainties on the input data points were assumed. The same assumption was also used when generating the data replicas, see Sec. IV.

When not taking into account the CI contribution, the resulting sets of PDFs, referred to as ZCIPDFs in the following, are in good agreement with HERAPDF2.0 fit results obtained within the HERAFitter framework [19]. The experimental uncertainties on the fitted model parameters and on the predictions from ZCIPDF, resulting from the uncertainties of the input HERA data, were defined by the criterion $\Delta \chi^2 = 1$. This takes into account statistical uncertainties and also correlated and uncorrelated systematic uncertainties of the combined HERA data, see Eq. (3).

**B. Modeling uncertainties**

Following the approach used for the HERAPDF2.0 fit [1], the uncertainties on the ZCIPDF fit due to the choice of the form of the parametrization and the model settings were evaluated by varying the assumptions. Two kinds of parametrization uncertainties were considered: the variation in the fit starting scale, $\mu^2_{fs}$, and the addition of parameters in the parton-density parametrization. The parameters $D$ and $E$, defined in the previous HERA analysis [1], were added separately for each PDF. The final parametrization uncertainty on the fitted coupling constant was taken to be the largest of the resulting deviations. The variations of charm and beauty mass parameters, $M_c$ and $M_b$, respectively, were chosen in accordance with the mass estimation from HERAPDF2.0. The variation of the strange-sea fraction, $f_s$, was chosen to span the ranges between a suppressed strange sea [20,21] and an unsuppressed strange sea [22,23]. In addition to these model variations, the minimal $Q^2$ of the data points used in the fit, $Q^2_{\text{min}}$, was varied. A summary of the variations on the model settings is given in Table III.

For each fitted coupling, the differences between the central fit and the fits corresponding to the variations of $Q^2_{\text{min}}$, $f_s$, $M_c$, and $M_b$, and the largest parametrization uncertainty were added in quadrature, separately for positive and negative deviations, and represent the uncertainties of the input parameters for the fit and the variations considered to evaluate model and parametrization uncertainties.

| Variation                  | Nominal value | Lower limit | Upper limit |
|---------------------------|---------------|-------------|-------------|
| $Q^2_{\text{min}}$ [GeV$^2$] | 3.5           | 2.5         | 5.0         |
| charm mass parameter $M_c$ [GeV] | 1.47         | 1.41        | 1.53        |
| beauty mass parameter $M_b$ [GeV] | 4.5          | 4.25        | 4.75        |
| sea strange fraction $f_s$ | 0.4           | 0.3         | 0.5         |
| starting scale $\mu^2_{fs}$ [GeV$^2$] | 1.9          | 1.6         | 2.2         |
The total uncertainty was obtained by adding in quadrature the experimental and the modeling uncertainties.

C. Fit results

The ZCIPDF fit to the HERA inclusive data was extended by adding the CI coupling, \( \eta \) (or \( \eta_{\text{LQ}} \) for LQ models) as an additional fit parameter. Results of the simultaneous QCD + CI fit to the HERA inclusive data, in terms of the fitted coupling values, are presented in Tables I and II, for CI and heavy-LQ scenarios, respectively. Experimental, modeling and total uncertainties on the fitted coupling values were calculated following the HERAPDF2.0 approach, as described above. Also shown is the change of the \( \chi^2 \) value from the nominal SM fit, \( \Delta \chi^2 = \chi^2_{\text{SM+CI}} - \chi^2_{\text{SM}} \). For most of the considered CI scenarios, only one minimum was observed in the \( \chi^2 \) dependence on the coupling value. The VA model was the only case where two minima were observed, one for a positive and one for a negative coupling. Results for both minima are presented in Table I.

In most cases, correlations between PDF parameters and CI coupling values resulting from the QCD + CI fit are small. The largest correlations are observed between the CI coupling and the parameters \( B_{dL} \), \( B_{uL} \), and \( C_D \), used in the description of the valence quark, valence \( u \) quark and \( d \)-type antiquark distribution, respectively. Their absolute values reach 0.61 for CI models (\( \eta - B_{dL} \) correlation in the AA model) and 0.57 for LQ models (\( \eta - C_D \) correlation in the \( V^h_L \) model).

For six out of 13 considered CI scenarios and seven out of 14 heavy-LQ models, no significant improvement in description of the data was observed. The fits were consistent with \( \Delta \chi^2 \approx -1 \), expected for a reduction of the number of degrees of freedom. The fitted coupling values for these models are consistent with zero. However, there are also four models (three CI and one \(^4\) LQ scenario), which result in an improved description of the data, with \( \Delta \chi^2 < -4 \). The best description of the inclusive HERA data is obtained for the X6 model (\( \Delta \chi^2 = -6.01 \)) and the \( S^L_1 \) model (\( \Delta \chi^2 = -11.10 \)). The fit results for these models are compared with HERA NC DIS data in Figs. 1 and 2, respectively. Also indicated is the SM contribution to the NC DIS cross sections obtained from the QCD + CI fit.

Figure 1 shows that, for the X6 model, the determination of the proton PDFs is affected very little by the CI contribution; the SM part of the NC DIS cross sections extracted from the QCD + CI fit agree with the nominal ZCIPDF fit within the quoted PDF uncertainties. The change in the predicted NC DIS cross section is dominated by the CI contribution. The situation is different for the \( S^L_1 \) heavy-LQ model shown in Fig. 2, where the description of the proton PDFs is significantly affected when the heavy-LQ contribution is taken into account in the fit. As a result, the cross section prediction for NC \( e^+ p \) DIS due to \( \gamma/Z^0 \) exchange increases at the highest values of \( Q^2 \), \( Q^2 > 50000 \text{ GeV}^2 \), by about a factor of two. The virtual leptoquark exchange contribution to the NC \( e^+ p \) DIS cross section is much smaller than the change observed in the SM contribution. Moreover, it decreases the total cross section due to the negative interference with the SM part. The improvement in the description of the data for the \( S^L_1 \) heavy-LQ model is also due to the better agreement of the resulting predictions with the CC DIS data.

Table I also includes estimates of the modeling (and the resulting total) uncertainties on the fitted CI coupling values. For most of the models, the modeling uncertainties tend to be small, below the level of experimental uncertainties. However, they are significant for the three CI models, AA, X1 and X6, for which \( \Delta \chi^2 < -4 \). Most important are the choice of the \( Q^2_{\text{min}} \) parameter (used to select the input data set for the fit) and the inclusion of the additional \( D_{u_4} \) parameter \(^{[1]} \) in the valence \( u \)-quark density description. When the \( D_{u_4} \) parameter is added to the ZCIPDF, it results in a \( \Delta \chi^2 = -10.3 \). After the addition of the \( D_{u_4} \) parameter, the improvement in \( \chi^2 \) due to the CI

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\(^{4}\)The improvement observed for the \( V^h_L \) model is not considered, as it is obtained for an unphysical (negative) coupling value.
the technique of replicas.

Q

predicted NC
models were derived in a frequentist approach[24] using expected at large parametrization, an description achieved with this quite different ansatz is much using the bilog parametrization[18]. While the overall are sizeable, see Table II, they cannot explain the improvement in the description of the HERA data. The QCD inclusive data, for the

\[ \Delta \chi^2 \text{ term is reduced for the AA, X1 and X6 models, and it is maximal for the VA model at } \Delta \chi^2 = -4.6. \]

For the \( S_1^L \) LQ scenario, although modeling uncertainties are sizeable, see Table II, they cannot explain the improvement in the description of the HERA data. The QCD + \( S_1^L \) fits result in \( \Delta \chi^2 < -9 \) for all considered model and parametrization variations. The \( S_1^L \) contribution to the predicted NC \( e^- p \) DIS cross section increases at the highest \( Q^2 \) values. For \( e^+ p \) scattering, the increase is expected at large \( x \) values.\(^5\) A cross-check was also made using the bilog parametrization [18]. While the overall description achieved with this quite different ansatz is much worse than the description achieved with the HERAPDF parametrization, an \( S_1^L \) term of similar strength was found.

IV. LIMIT-SETTING PROCEDURE

The limits on the mass scales of the CI and heavy-LQ models were derived in a frequentist approach[24] using the technique of replicas.

A. Data set replicas

Replicas are sets of cross section values, corresponding to the HERA inclusive data set that are generated by varying all cross sections randomly according to their known uncertainties. For the analysis presented here, multiple replica sets were used, each covering cross section values on all points of the \( x, Q^2 \) grid used in the QCD fit. For assumed true values of the CI coupling, \( \eta^{\text{True}} \), replica data sets were created by taking the reduced cross sections calculated from the nominal PDF fit (with CI coupling \( \eta = 0 \)) and scaling them with the cross section ratio \( K_\text{CI} \) given by Eq. (2). This results in a set of cross section values \( m_0^i \) for the assumed true CI coupling \( \eta^{\text{True}} \). The values of \( m_0^i \) were then varied randomly within the statistical and systematic uncertainties taken from the data, taking correlations of systematic uncertainties into account. All uncertainties were assumed to follow a Gaussian distribution.\(^6\)

For each replica, the generated value of the cross section at the point \( i, \mu^i \), was calculated as

\[
\mu^i = \left[ m_0^i + \sqrt{\delta^2_{\text{stat}} + \delta^2_{\text{uncor}} \cdot r_i} \right] \cdot \left( 1 + \sum_j y_j^i \cdot r_j \right),
\]

where variables \( r_i \) and \( r_j \) represent random numbers from a normal distribution for each data point \( i \) and for each source of correlated systematic uncertainty \( j \), respectively.

The approach adopted was to generate large sets of replicas and use them to test the hypothesis that the cross sections are consistent with the SM predictions or that they were modified by a fixed CI coupling according to Eq. (2). The fitted \( \eta \) values from the replicas, \( \eta^{\text{Fit}} \), were used as a test statistics and compared to the corresponding value \( \eta^{\text{Data}} \) determined from a fit to the data.

To quantify the statistical consistency of the fit results with the SM expectations, the probability that an experiment assuming the validity of the SM (replicas generated with \( \eta^{\text{True}} = \eta^{\text{SM}} = 0 \)) would produce a value of \( \eta^{\text{Fit}} \) greater than (or less than) that obtained from the data was calculated:

\[
P_{\text{SM}} = \begin{cases} 
\begin{align*}
\frac{1}{2} & \text{ for } \eta^{\text{Data}} > 0, \\
\frac{1}{2} & \text{ for } \eta^{\text{Data}} < 0,
\end{align*}
\end{cases}
\]

where the probability \( p \) was calculated from the distribution of \( \eta^{\text{Fit}} \) values for a large set of generated SM replicas.

\(^5\)This is due to an additional kinematic factor of \( (1 - y)^2 \) multiplying the LL scattering amplitude for NC \( e^\pm p \) DIS.

\(^6\)It was verified that using a Poisson probability distribution for producing replicas at high \( Q^2 \), where the event samples are small, and using the \( \chi^2 \) minimization for these data did not change the results.
B. Constraining BSM scenarios

While for LQ models only positive $\eta_{LQ}$ values were considered, in the case of the CI scenarios, coupling limits were calculated separately for positive and negative $\eta$ values. The upper (lower) 95% C.L. limit on the positive (negative) coupling, $\eta^+$ ($\eta^-$), for a given scenario was determined as the value of $\eta^{\text{true}}$ for which 95% of the replicas produced a fitted coupling value, $\eta^{\text{fit}}$, larger (smaller) than that found in the data, $\eta^{\text{data}}$, see Eq. (5). The corresponding mass-scale values ($\Lambda^+$ and $\Lambda^-$ for CI scenarios or $M/\lambda$ for LQ models) will be referred to as mass-scale limits. A similar procedure [7] was also used to calculate the expected limit values, which were defined by comparing replica fit results with $\eta^{\text{SM}} \equiv 0$ instead of $\eta^{\text{data}}$.

To take modeling uncertainties into account, the limit-calculation procedure was repeated for model or parametrization variations resulting in the highest and the lowest $\eta^{\text{data}}$ values for each model. The weakest of the obtained coupling limits was taken as the result of the analysis and used to calculate the final mass-scale limits. This is clearly the most conservative approach, which is motivated by the difficulty in defining the underlying probability distribution for some of the considered modeling variations.

The expected limits are not sensitive to the modeling variations because these mainly affect the data fit results ($\eta^{\text{data}}$ values) and the expected values do not depend on $\eta^{\text{data}}$ (replica fit results are compared to $\eta^{\text{SM}} \equiv 0$). Therefore, these variations were not considered for the expected limits.

For each CI and LQ scenario, at least 3000 Monte Carlo replicas were generated and fitted for each value of $\eta^{\text{true}}$. When using xFitter to perform replica fits, the inclusion of more models in the analysis was limited by the processing time. To facilitate efficient processing of replica data, a simplified fit method, based on the Taylor expansion of the cross section predictions in terms of PDF parameters was developed, which reduced the processing time by almost two orders of magnitude [25].

V. RESULTS

The probabilities $p_{\text{SM}}$ [Eq. (5)] calculated for the considered CI scenarios with the SM replica sets are presented in Table IV. The statistical approach based on Monte Carlo replicas confirms the observations described in Sec. III C, based on the $\Delta \chi^2$ values. For six CI models (LR, RL, VV, X2, X4, and X5), $p_{\text{SM}}$ is above 20%, corresponding to less than a $1\sigma$ deviation from the nominal fit result ($\eta^{\text{SM}} = \eta^{\text{SM}} \equiv 0$). For four models (LL, LR, VA, and X3), the data fit results are reproduced by the SM replicas with 3%–7% probability, corresponding to about a

| Table IV. Contact-interaction coupling values determined from the fit to the HERA inclusive data, $\eta^{\text{data}}$, and probabilities to obtain larger absolute coupling values from the fit to the SM replica, $p_{\text{SM}}$, for the considered CI models. Also shown are the 95% C.L. limits on the CI couplings obtained from the presented analysis without (exp) and with (exp + mod) model and parametrization variations. Lower and upper coupling limits, $\eta^-$ and $\eta^+$, are calculated separately for negative and positive coupling values, respectively. The 95% C.L. upper limits on the compositeness scale, $\Lambda^+$ and $\Lambda^-$, correspond to the scenarios with positive and negative coupling values, respectively. The same coupling structure applies to all quarks. Only positive coupling values are allowed at 95% C.L. for the X1 model, and for the AA model when modeling uncertainties are not taken into account, while for the X6 model only negative coupling values are allowed. For the VA model, the fit range is restricted to negative or positive couplings for lower and upper limit calculations, respectively (see text for details). |

| Model | $\eta^{\text{data}}$ (TeV$^{-2}$) | $p_{\text{SM}}$ (%) | 95% C.L. coupling limits (TeV$^{-2}$) | 95% C.L. mass scale limits (TeV) |
|-------|-----------------|----------------|---------------------------------|-----------------|
|       |                 |                 | Measured (exp) | Measured (exp + mod) | Expected                    | Measured (exp + mod) | Expected                    |
| LL    | 0.305           | 7.0             | $-0.033$     | $0.610$               | $-0.077$ | $0.616$ | $-0.367$ | $0.319$ | 12.8 | 4.5 | 5.9 | 6.3 |
| RR    | 0.338           | 5.9             | $-0.017$     | $0.649$               | $-0.058$ | $0.656$ | $-0.390$ | $0.337$ | 14.7 | 4.4 | 5.7 | 6.1 |
| LR    | $-0.084$        | 34              | $-0.514$     | $0.250$               | $-0.565$ | $0.413$ | $-0.388$ | $0.313$ | 4.7  | 5.5 | 5.7 | 6.3 |
| RL    | $-0.040$        | 42              | $-0.464$     | $0.299$               | $-0.503$ | $0.444$ | $-0.397$ | $0.302$ | 5.0  | 5.3 | 5.6 | 6.5 |
| VV    | 0.041           | 25              | $-0.058$     | $0.135$               | $-0.065$ | $0.155$ | $-0.101$ | $0.097$ | 13.9 | 9.0 | 11.2 | 11.4 |
| AA    | 0.326           | 0.6             | $0.530$      | $-0.051$              | $0.700$   | $-0.200$ | $0.207$   | $15.7$    | 4.2  | 7.9 | 7.8 |
| VA    | $-0.594$        | 5.8             | $-0.888$     | $0.947$               | $-0.969$ | $0.997$ | $-0.723$ | $0.719$ | 3.6  | 3.5 | 4.2 | 4.2 |
| X1    | 0.682           | 0.4             | $1.020$      | $1.230$               | $-0.435$ | $0.418$ | $3.2$     | $5.4$     | 5.5  | 5.5 |
| X2    | 0.089           | 24              | $-0.113$     | $0.269$               | $-0.125$ | $0.310$ | $-0.206$ | $0.184$ | 10.4 | 6.4 | 7.8 | 8.3 |
| X3    | 0.158           | 7.3             | $-0.018$     | $0.320$               | $-0.039$ | $0.324$ | $-0.183$ | $0.166$ | 17.9 | 6.2 | 8.3 | 8.7 |
| X4    | $-0.029$        | 39              | $-0.230$     | $0.144$               | $-0.243$ | $0.223$ | $-0.194$ | $0.170$ | 7.2  | 7.5 | 8.0 | 8.6 |
| X5    | 0.079           | 27              | $-0.129$     | $0.263$               | $-0.138$ | $0.303$ | $-0.212$ | $0.188$ | 9.5  | 6.4 | 7.7 | 7.7 |
| X6    | $-0.786$        | 0.3             | $-1.130$     | $-1.310$              | $-0.454$ | $0.415$ | $3.1$     | $5.3$     | 5.5  | 5.5 |

H. ABRAMOWICZ et al.  

PHYS. REV. D 99, 092006 (2019)
2σ difference. However, for the three scenarios (AA, X1 and X6) with Δχ² < -4, p_{SM} is below 1%. This confirms that the differences between the HERA data and the SM predictions described by the additional CI contribution in the fit are unlikely to be due to statistical fluctuations only. As already discussed in Sec. III C, the effect can be explained to some extent by the modeling uncertainties, in particular by the deficiencies in the functional form used for the PDF parametrization.

Also shown in Table IV are the 95% C.L. limits on the coupling values, η⁻ and η⁺, for different CI models. Limits calculated without (exp) and with (exp + mod) model and parametrization variations, as described above, are compared to the expected coupling limits in Fig. 3. Coupling limits can also be translated into limits on the compositeness scales for the considered CI scenarios, also included in Table IV.

For most of the CI scenarios considered, the interference term gives a significant contribution to the cross section and the interference term is much smaller than the direct CI contribution. However, in the case of the V A model, the contribution from the sign of the CI coupling is well constrained in the fit. The LQ coupling values determined from the fit to the HERA inclusive data, η_{LQ}^\text{Data}, and the probabilities p_{SM} are summarized in Table V together with the coefficients d_{ij}, describing the CI coupling structure of the considered LQ models. Also shown are the 95% C.L. upper limits on the

![Diagram 3](image3.png)

**FIG. 3.** Limits on the CI coupling strength, $\eta = \pm 4\pi/\Lambda^2$, evaluated at 95% C.L. Compared are the limits calculated without (endpoints of dark upper bars) and with (light upper bars) modeling uncertainties, and the expected limits (lower bars). Limits are calculated separately for positive and negative coupling values (see text for details).

![Diagram 4](image4.png)

**FIG. 4.** HERA (a) $e^+p$ and (b) $e^-p$ NC DIS data, relative to the SM expectations based on the ZCIPDF fit to the HERA inclusive data, compared to expectations from the VV and AA contact-interaction models with the effective mass scale for positive ($\Lambda^+$) and negative ($\Lambda^-$) couplings corresponding to the 95% C.L. limits. The same four models are shown on both plots. The bands represent the total uncertainty on the ZCIPDF fit predictions.
reproducing the fit result with SM replicas, the HERA data can be obtained and the probability of 5% is also obtained for the still below 5% for both models. A probability of less than both models are excluded at 95% C.L.

Limits calculated without (exp) and with (exp + mod) modeling uncertainties are compared with the expected limits. For the $S_0^L$ and $V_0^L$ models, all positive coupling values are excluded at 95% C.L.

| Model | Coupling structure | $\eta_{LQ}^{\text{Data}}$ (TeV$^{-2}$) | $\rho_{SM}$ (%) | $\lambda_{LQ}/M_{LQ}$ 95% C.L. limits (TeV$^{-1}$) | Measured | Expected |
|-------|-------------------|--------------------------------------|----------------|-----------------------------------------------|----------|----------|
|       |                   |                                      |                | (exp) (exp + mod)                             |          |          |
| $S_0^L$ | $a_{LL}^{ee} = +\frac{1}{2}$ | -0.258                                 | 9.0            | 0.25 (exp) 0.28 (exp + mod)                    | 0.56     |          |
| $S_0^R$ | $a_{RR}^{ee} = +\frac{1}{2}$ | 0.533                                | 5.5            | 1.02 (exp) 1.03 (exp + mod)                    | 0.72     |          |
| $S_0^L$ | $a_{LR}^{ee} = -\frac{1}{2}$ | -2.561                                | 1.8            |                                      | 1.71     |          |
| $S_{1/2}^L$ | $a_{LL}^{ee} = -\frac{1}{2}$ | 0.054                                | 43             | 0.80 (exp) 0.83 (exp + mod)                    | 0.76     |          |
| $S_{1/2}^R$ | $a_{RR}^{ee} = +\frac{1}{2}$ | 0.112                                | 39             | 0.99 (exp) 1.04 (exp + mod)                    | 0.92     |          |
| $S_{1/2}^L$ | $a_{LR}^{ee} = -\frac{1}{2}$ | 0.464                                | 38             | 1.51 (exp) 1.66 (exp + mod)                    | 1.39     |          |
| $S_1^L$ | $a_{LL}^{ee} = +\frac{1}{2}$ | 0.974                                | <0.01          | 1.16 (exp) 1.18 (exp + mod)                    | 0.62     |          |
| $V_0^L$ | $a_{LL}^{ee} = -1$ | -0.325                                | 0.5            |                                      | 0.44     |          |
| $V_0^R$ | $a_{RR}^{ee} = -1$ | 1.280                                | 1.8            | 1.44 (exp) 1.47 (exp + mod)                    | 0.99     |          |
| $V_0^L$ | $a_{LR}^{ee} = -1$ | -0.267                                | 5.5            | 0.06 (exp) 0.18 (exp + mod)                    | 0.53     |          |
| $V_{1/2}^L$ | $a_{RR}^{ee} = +1$ | -0.232                                | 38             | 1.12 (exp) 1.19 (exp + mod)                    | 1.29     |          |
| $V_{1/2}^R$ | $a_{LR}^{ee} = +1$ | -0.056                                | 39             | 0.55 (exp) 0.67 (exp + mod)                    | 0.57     |          |
| $V_1^L$ | $a_{LL}^{ee} = -1, a_{LR}^{ee} = -2$ | 0.029                                | 32             | 0.39 (exp) 0.41 (exp + mod)                    | 0.49     |          |

The ratio of the Yukawa coupling to the leptoquark mass, $\lambda_{LQ}/M_{LQ}$. Limits calculated without (exp) and with (exp + mod) model and parametrization variations are compared with the expected 95% C.L. limits on $\lambda_{LQ}/M_{LQ}$ in Fig. 5.

For the $S_1^L$ model, an improvement in the description of the HERA data can be obtained and the probability of reproducing the fit result with SM replicas, $\rho_{SM}$, is below 0.01%. For the $V_0^L$ model, the probability $\rho_{SM}$ is 1.8%, which means that for both models $\eta_{LQ} = 0$ is excluded at 95% C.L. When modeling uncertainties are taken into account, the corresponding $\rho_{SM}$ values increase, but are still below 5% for both models. A probability of less than 5% is also obtained for the $S_0^R$ and $V_0^L$ models. However, the fit gives unphysical (negative) coupling values so that both models are excluded at 95% C.L.

Assuming the Yukawa coupling value, $\lambda_{LQ} = 1$, the corresponding lower limits on the leptoquark mass vary between 0.66 TeV for the $S_{1/2}^L$ model and 16 TeV for the $V_0^L$ model. When modeling uncertainties are included, the limits vary between 0.60 TeV and 5.6 TeV. In Fig. 6, the measured $Q^2$ spectra of the HERA $e^+p$ and $e^-p$ data, relative to the SM predictions calculated using ZCIPDF, are compared with the expectations for the $S_1^L$ and $V_0^L$ leptoquark models which correspond to the limits on the ratio of the leptoquark Yukawa coupling to the leptoquark mass shown in Fig. 5.

Two types of limits can be set on the considered BSM scenarios at the LHC. Direct searches for LQ pair-production result in $M_{LQ}$ limits for first-generation leptoquarks in the TeV range [26,27]. These limits do not depend on the leptoquark Yukawa coupling and cannot be directly compared to the presented HERA results. Independent limits on the ratio of the Yukawa coupling to the LQ mass, $\lambda_{LQ}/M_{LQ}$, as well as limits on the CI mass scales can be set from the analysis of the dilepton production in the Drell–Yan process. The diagram for this process corresponds to that describing NC DIS at HERA and the BSM contributions can be searched for in exactly the same CI framework.

A comparison of the present results with limits obtained by the ATLAS [28] and CMS [29] collaborations at the LHC, based on dilepton data collected at 13 TeV, is presented in Table VI. Only the four CI models shown were considered in the analyses of the LHC data. It is clear that, for these models, the statistical sensitivity of the LHC experiments is much higher than that of the HERA inclusive data. However, the systematic uncertainties...
FIG. 5. Upper 95% C.L. limits on the LQ coupling strength, \( \eta_{LQ} = \frac{\lambda_{LQ}^2}{M_{LQ}^2} \). Compared are the limits calculated without (dark upper bars) and with (light upper bars) modeling uncertainties, and the expected limits (lower bars).

FIG. 6. HERA (a) \( e^+ p \) and (b) \( e^- p \) NC DIS data, relative to the SM expectations based on the ZCIPDF fit to the HERA inclusive data, compared to expectations from the \( S_1^L \) and \( V_0^R \) leptoquark models with the ratios of the LQ Yukawa couplings to the LQ mass, \( \lambda/M \), corresponding to the 95% C.L. limits. The same two models are shown on both plots. The bands represent the total uncertainty on the ZCIPDF fit predictions.

TABLE VI. Comparison of the 95% C.L. limits on the compositeness scale, \( \Lambda \), obtained from the ZEUS analysis of the HERA inclusive data with limits on \( eeeq \) CI resulting from the analysis of the dilepton mass spectra at 13 TeV LHC presented by the ATLAS Collaboration [28] and by the CMS Collaboration [29]. For the ATLAS experiment, limits that were obtained in a Bayesian framework with an assumed uniform positive prior in \( 1/\Lambda^2 \) are shown.

| Coupling structure | HERA | ATLAS | CMS |
|--------------------|------|-------|-----|
| Model              | \( \varepsilon_{LL}, \varepsilon_{LR}, \varepsilon_{RL}, \varepsilon_{RR} \) | \( \Lambda^- \) | \( \Lambda^+ \) | \( \Lambda^- \) | \( \Lambda^+ \) |
| LL                 | [+1, 0, 0, 0] | 12.8 | 4.5 | 24 | 37 | 16.8 | 24.0 |
| RR                 | [0, 0, 0, +1] | 14.7 | 4.4 | 26 | 33 | 16.9 | 23.8 |
| LR                 | [0, +1, 0, 0] | 4.7 | 5.5 | 26 | 33 | 21.3 | 26.4 |
| RL                 | [0, 0, +1, 0] | 5.0 | 5.3 | 26 | 33 |       |     |

resulting from the proton PDFs can be underestimated, as the possible bias in the parametrization was not taken into account.

VI. CONCLUSIONS

The HERA combined measurement of inclusive deep inelastic cross sections in neutral and charged current \( e^\pm p \) scattering has been used to search for possible deviations from the Standard Model predictions within the \( eeeq \) contact-interaction approximation. The procedure was based on a simultaneous fit of PDF parameters and the CI coupling. Limits on the CI couplings and probabilities for the SM predictions were obtained with Monte Carlo replicas. These were used to set limits on the CI compositeness scales, \( \Lambda \), and limits on the ratios of the leptoquark Yukawa coupling to the leptoquark mass, \( \lambda_{LQ}/M_{LQ} \).

The addition of terms effective at high \( Q^2 \), such as those found in the CI and LQ models described above, reduces the tension between high-\( Q^2 \) and low-\( Q^2 \) data previously observed in the HERAPDF2.0 analysis. For the AA, VA, X1 and X6 models, the QCD + CI fits provide improved descriptions of the HERA inclusive data, corresponding to a difference from the SM predictions at the level of up to 2.7\( \sigma \) (SM probability of 0.3% for the X6 model). A similar effect is observed for the \( S_1^L \) and \( V_0^R \) leptoquark models, which give an improved description of the HERA inclusive data, corresponding to a difference from the SM predictions at a level of about 4\( \sigma \) and about 2\( \sigma \), respectively. These deviations are unlikely to result from statistical fluctuations alone, but might be explicable by a combination of modeling uncertainties in the fitting procedure and statistical fluctuations. Since an unambiguous deviation from the SM cannot be established with the HERA data, limits for CI compositeness scales and LQ mass scales were set that are in the TeV range.
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