Research Article

A Model for the Spacing of Quicklime Pile to Treat High Water Content Loess

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There has been a long history for foundation treatment by quicklime pile, but as for establishing a more precise model formula used by actual construction, further research is needed to be done at present. Therefore, how to quantitate the factors affecting pile spacing is of great reference value for both actual constructions and theoretical studies. Based on the reference formula for handling weak foundation by lime pile and the practical problems in the western region, mathematical model analysis method is used to get a new model for high water content loess foundation treatment after considering the factors such as pile expanding, construction method, piles arrangement, and calcium oxide content. In this model, pile spacing coefficient is created and the model formula for different construction methods and different pile arrangements is also given. As a result, the reference formula used in high water content loess is somewhat conservative. The new model is also verified to be rational by the actual works at the end of the paper.

1. Introduction

Loess, which is an aeolian silt sediment with variable amounts of sand and clay, is often loosely cemented by calcite (CaCO₃) and widely distributed in Northwest China and other regions in the world. The natural loess, despite its relatively low dry density (1.10–1.68 g/cm³) and large void ratio usually (0.67–1.13, [1]), as shown in Table 1, can have a relatively stable internal structure due to weak bonding among particles (i.e., metastable). It is well known that loess soils are water-sensitive [2–6]: that is, when water content increases (e.g., after rainfall or irrigation), a loess soil often exhibits a significant decrease in shear strength. For example, the influence of water content on the shear strength of one of the loess soils in Shaanxi Province of China can apparently be seen from reference [1]. High water content loess soils have always been a challenge for geotechnical engineers because such soils often have a very low bearing capacity and their high water content also makes mechanical compaction ineffective. According to previous studies in the literature [7], the friction angle and bearing capacity of loess almost increase linearly with the decrease in water content and void ratio. Although currently there are several methods to treat high water loess soils, for example, CFG pile (cement and fly ash gravel pile) [8] and stone pile [9], these methods tend to be more costly, and more importantly, these piles are not effective in reducing high water content in loess soils. As mentioned above, both water content and dry density have significant effects on the shear strength and the bearing capacity of loess soils, and the key to reinforce loess soils is how to reduce their water content and increase dry density [10]. In this regard, quicklime pile appears a promising solution to treating high water content loess due to its following characteristics: CaO can absorb water by hydration reaction, during which CaO itself swells and becomes slaked lime (Ca(OH)₂) which in turn densifies the adjacent soils and increases their dry density.

Quicklime (CaO) pile is essentially a column filled with compacted or pneumatically densified lime, which has been successfully used in reinforcing soils [11, 12]. Quicklime piles are often installed in either a triangular or rectangular pattern. The spacing [13–17] between lime piles needs to be
2. Reinforcement Mechanisms of Quicklime Piles

The mechanisms of soil reinforcement with quicklime piles include three main categories: soil densification due to water content loss and compaction due to swelled quicklime piles, pile strengthening, and composite foundation associated with quicklime pile-soil reactions.

The basis to compute the spacing of quicklime piles is the hypothesis that the amount of water lost in the soil is equal to the amount of water increase in quicklime piles. The water lost from the soil is absorbed by lime pile. In fact, two steps are involved during quicklime hydration process: first, lime and water react to yield hydrated lime, during which 1 unit mass CaO absorbs 0.32 unit mass water according to the following chemical reaction formula, with the molecular weight of CaO as the reference:

$$\text{CaO} + \text{H}_2\text{O} = \text{Ca(OH)}_2 + 64.9\text{kJ/mol}$$  \hfill (3)

The molecular weight for CaO, H2O, and Ca(OH)2 is 56, 18, and 74 g/mol and their weight ratio is 1, 0.32, and 1.32, respectively.

Secondly, dry Ca(OH)2 continues to physically absorb water mainly because of the capillary attraction [19] in the Ca(OH)2. This capillary suction will provide a driving force for transferring water from the soil to the pile. This process will reach equilibrium when the dry Ca(OH)2 absorbs a certain amount of water. The previous study indicated that an appreciable amount of water is absorbed during this process [20]. There is an evidence that quicklime pile is neither in the air nor under groundwater in the situation as presented in this paper. However, the average water content of the Ca(OH)2 (100%) can be still used when absorbing water in the air. Note that this is under our hypothesis that the quicklime pile can contact to the air in the soil. Hence, 1 unit weight CaO can absorb 1.64 unit weight water.

The design of the pile spacing is very important. If the pile spacing is too large, water in the soil would not be completely absorbed by the quicklime pile, and, if it is too small, more quicklime piles would be installed which is definitely a waste of time and materials. Hence, the maximum pile spacing is derived herein. It is easy to get the total amount of water one quicklime pile can absorb:

$$m_l = \frac{\pi D^2 \rho_d H \cdot 1.64}{4},$$  \hfill (4)

where $\rho_d$ is the bulk density of quicklime, usually 0.72–1.13 g/cm³, 1.64 is discussed above, and $H$ is the quicklime pile length.

The total mass of water loss from the affected soil region depends on the quicklime pile arrangement (usually in construction, there are two types of pile arrangements: one is called triangular arrangement (see Figure 1(a)) and the other is square arrangement (see Figure 1(b))). The affected soil regions by quicklime piles are illustrated in Figures 1(a) and 1(b) for triangular and square patterns, respectively.

So for the triangular arrangement and the square arrangement, the total mass of water loss from the affected soil region is presented as follows:

$$m_t = \frac{\sqrt{3}}{2} \Delta w S^2 \rho_d$$ (for the triangular arrangement), \hfill (5)

$$m_t = \Delta w S^2 \rho_d$$ (for the square arrangement), \hfill (6)

where $\Delta w$ is the water content change in the soil after the quicklime pile reinforcement and $S$ is the pile spacing.

The water lost from this affected soil region can be completely absorbed by the quicklime piles only if $m_t \geq m_l$, which yields the upper limit of the center-to-center spacing of quicklime piles. From equations (4)–(6), the following equations can be obtained:

| Water content | Very low | Low | High | Very high | Saturated |
|---------------|---------|-----|------|-----------|-----------|
| Cohesion (kPa) | >120    | 80–110 | 40–80 | 10–40 | <10 |
| Friction angle ($) | >33     | 29–33 | 24–29 | 23–24 | <23 |
\[ S \leq 1.220 \cdot D \sqrt{\frac{\Delta \rho_d}{\Delta w \rho_d}} = L_s D \text{ (for the triangular arrangement),} \]
\[ S \leq 1.135 \cdot D \sqrt{\frac{\Delta \rho_d}{\Delta w \rho_d}} = L_s D \text{ (for the square arrangement),} \]

where \( L_s \) is the maximum quicklime pile spacing coefficient, which is larger than or equal to the designed quicklime pile spacing in order to ensure that the water loss from the reinforced soil is completely absorbed by the adjacent quicklime piles.

The quicklime pile will swell itself after absorbing water. Equations (1) and (2) do not consider this effect, but in this paper, this gap has been covered. After the expansion of the quicklime pile by absorbing water which is lost from the stabilized soil, the volume of a quicklime pile will increase to \( k_v \) times:

\[ 0.25\pi D'^2 H = k_v 0.25\pi D^2 H, \]

where \( D \) is the initial pile diameter, \( D' \) is the pile diameter after its expansion, and \( k_v \) is the volume expansion coefficient of quicklime piles. The value range of the expansion coefficient \( k_v \) is discussed below. Lime pile expansion can be considered, which consists of two parts: one part is due to the absorbed water, which is designated as \( k_{v1} \), and depends on the fraction of the quicklime because sometimes sand or fly ash is added to the quicklime to make the pile together. So \( k_{v1} \) here is 1.65 (quicklime) and 1.33 (ash:lime = 3:7),

**Figure 1:** Schematic of quicklime piles installed in a triangular arrangement (a) and a square arrangement (b) and the affected soil range (\( D \) is the initial pile diameter, \( D' \) is the pile diameter after expansion, and \( S \) is the pile spacing).
respectively, while the other is the expansion associated with pile driving, which is designated as $K_{dr}$. Because vibration always happens during the pile driving, as a result, the hole in construction would be little bigger than the design value because quicklime lump is filled into the hole that will be hard to exactly control the pile diameter. Gong [21] suggested that the actual pile diameter $D_0 = [(1.1 \sim 1.2)+30 (\text{mm})]D$. Suppose the pile diameter becomes 1.2 times under driving vibration, in this case $K_{dr} = 1.2^2 = 1.44$. Therefore, the expansion coefficient $k_v = k_{v1}k_{v2} = 1.92 \sim 2.38$.

Also, a quicklime pile itself can support part of the structural loading, especially after the pile is strengthened by the following chemical reaction processes: from $\text{CaO}$ to $\text{Ca(OH)}_2$, and then to $\text{CaCO}_3$, which has a high strength of 300–500 kPa according to the previous laboratory test [12]. Due to the difference in stiffness between the quicklime pile and the surrounding loess soil, a stress concentration occurs, with a higher stress applied on the quicklime pile than that on the surrounding soil. Thus, the composite quicklime pile-soil forms a stronger foundation. Although ion migration occurring between lime pile and clay soils plays a large role in reinforcing the whole composite foundation, loess soil has limited clay mineral materials and the reinforcement mechanism associated with ion migration of quicklime piles is not relevant and not considered for the case of loess soils.

3. Mathematical Models for Determining the Center-to-Center Spacing of Quicklime Piles

Based on the reinforcement mechanisms in loess soils by quicklime piles, mathematical models for determining the center-to-center spacing of quicklime piles are presented in this section, which consider the changes of water content and dry density of the stabilized soil before and after the treatment.

3.1. Center-to-Center Spacing for a Triangular Pattern. As illustrated in Figure 1 for a triangular pattern, one-sixth of a quicklime pile affects one-third of the soil in the triangular area enclosed by quicklime piles. Herein, two triangle regions are taken as the calculation area (Figure 1(a)). As for construction, two installation methods are considered: one method is called boring installation, which involves digging a hole (initial pile diameter) and getting the soil out from the hole and then refilling the hole with quicklime, and the other is called immersing installation method, in which a hollow tube is pushed into the soil to the required depth and quicklime is forced into the tube under pressure as it is withdrawn, and in this case, the soil is still in the ground [10]. So for the first installation method, the total mass of the soil before compaction in our calculation region (that enclosed within the two triangles formed by the adjacent quicklime piles as shown in Figure 1(a)) is calculated as follows:

$$m = \left(\frac{\sqrt{3}}{2}S^2 - \frac{\pi D^2}{4}\right)H\rho_d (1 + w)$$

(for the boring installation method),

and for the second installation method, the total mass is given by

$$m = \frac{\sqrt{3}}{2}S^2 H\rho_d (1 + w)$$

(for the immersing installation method),

where $m$ is the total mass of the soil before compaction; $S$ is the center-to-center pile spacing; $H$ is the quicklime pile length; $\rho_d$ is the initial soil dry density; and $w$ is the initial soil water content.

After the soil is stabilized by quicklime piles, the total mass of the soil for both the two installation methods can be calculated from the following equation in which the volume expansion of quicklime piles and the water loss from the stabilized soil are considered:

$$m' = \left(\frac{\sqrt{3}}{2}S^2 - \frac{\pi D^2}{4}\right)H\rho_d' (1 + w'),$$

where $m'$ is the total mass of the soil after compaction; $\rho_d'$ is the required soil dry density; and $w'$ is the final water content of the stabilized soil.

So from equations (3), (9), (11), and (12), the center-to-center quicklime pile spacing formula for the boring installation method can be calculated from equation (8), and from equations (4)–(7), the pile spacing formula (14) for the immersing installation method is obtained as follows:

$$S = 0.9523 \sqrt{\frac{\rho_d - k_v\rho_d'}{\rho_d - \rho_d}} D = L_p D$$

(for the boring installation procedure),

$$S = 0.9526 \sqrt{\frac{k_v\rho_d'}{\rho_d - \rho_d}} D = L_p D$$

(for the immersing installation procedure),

where $L_p$ is the quicklime pile spacing coefficient, which is convenient for the design of quicklime piles when their diameter is known. Note that $L_p$ should be less than $L_s$ during the design process because the water should be completely absorbed by the quicklime pile.

3.2. Center-to-Center Spacing for the Square Pattern. In this case, a pile can reinforce the soil in the square region indicated in Figure 1(b). Based on the similar analysis to that for the triangular layout pattern, the pile spacing formulas are yielded as follows:

$$S = 0.8662 \sqrt{\frac{\rho_d - k_v\rho_d'}{\rho_d - \rho_d}} D$$

(for the boring installation procedure),

$$S = 0.8662 \sqrt{\frac{k_v\rho_d'}{\rho_d - \rho_d}} D$$

(for the immersing installation procedure).
4. Applications and Discussions

To illustrate the difference in center-to-center spacing of quicklime piles among different spacing formulas, an example is discussed here with the following parameters: an expansion coefficient of 2.15 and the initial dry density ranging from 1.2 to 1.35 g/cm³, with the calculated spacing plotted in Figure 2 for different formulas and different pile arrangement and different construction methods.

It can be seen from Figure 2 that, in both square and triangular arrangement methods, the pile spacing coefficients in the boring method (equations (8) and (10)) are larger than those in the immersing method (equations (9) and (11)). It also shows that pile spacing coefficient in a triangle pattern is larger than that in a square pattern. That is to say, for the same pile diameter, the number of total piles using the immersing method is less than that using the boring method, and triangular arrangement also makes the total pile number less. This gives us two ideas: first, the former law (equations (1) and (2)) is conservative for loess soil, and second, the immersing construction method is more economical. In addition, when using the immersing method, loess with high water content need not to be drilled out, which is environmentally friendly because high water content loess is very sticky wherever it piled.

Next, the volume of the soil reinforced by the same amount of lime using different layout patterns is calculated as follows: \( V = K_i D^2 H \), \( i = s, t \), and \( j = 1, 2 \), where \( K_{ij} \) is the volume coefficient, subscript 1 stands for formula (1), 2 for formula (2), \( s \) for triangular arrangement, and \( t \) for square arrangement. For example, \( K_{1t} \) stands for the reinforced soil volume based on formula (1) using the triangular arrangement. In order to check the spacing of quicklime piles determined from the proposed formulas (from equations (3) to (6)), a case history in Yangling, Shaanxi, P.R.C., is analyzed using the model this paper presented. Quicklime piles were employed to treat the foundation area of \( 60 \times 16 \) m² of a 6-floor residential building. The building was constructed in 1996, and the quicklime pile-treated foundation performed well since then. The bearing capacities before and after the treatment are 115 and 270 kPa, respectively [22].

The groundwater level is about 50 meters below the ground surface, and the physical and mechanical properties of soil are shown in Table 2.

The project above is conducted by the boring method [23], and the piles, with 100% quicklime, were arranged in a square pattern. And the required dry density of this foundation is 1.65 g/cm³. From the physical properties summarized in Table 2, and here \( k_r = 2.38 \) based on the previous discussion, the pile spacing coefficient is \( L_p = 0.8862 \sqrt{(\rho_d - k_r \rho_d' / \rho_d - \rho_s')} = 2.75 \leq L_s \). Note that here \( L_p = 2.75 \) should be less than \( L_s \). So the bulk density of the quicklime should be controlled in the construction process (in the lower right of the black line, \( L_p < L_s \)). In the actual construction, the pile diameter was 0.18 m, the pile spacing was set to 0.5 m empirically, and the pile spacing coefficient is 0.5/0.18 = 2.78, which is pretty similar to the model results proposed here and also indicates that the equations in this paper are reasonable and safe to the construction. If equation (2) is used, the pile spacing would have been \( S = 0.89 D \sqrt{(\rho_d' / \rho_d - \rho_s')} = 0.41 \) m. This means 19.5% more quicklime would have been used to reinforce the foundation and longer quicklime installation time.

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**Table 2: Physical and mechanical properties of soil.**

| Soil depth (m) | Water content \( w \) (%) | Dry density \( (\rho_d' / g \cdot cm^{-3}) \) | Void ratio \( (e) \) | Specific gravity \( (G_s) \) |
|---------------|--------------------------|------------------|----------------|------------------|
| 3.5~5.5       | 24~28                    | 1.31              | 1.06           | 2.70             |
| 5.5~7.5       | 22~24                    | 1.50              | 1.01           | 2.71             |
The relation of pile spacing and initial water content in empirical value (0.5 m), existing model (equations (1) and (2)), and the new model presented in this paper is shown in Figure 3. Due to both safe and economical requirements in practical engineering, choosing the suitable pile spacing is of great importance. If the safety requirement is met in one engineering, it is recommended that the bigger pile spacing should be chosen. The empirical value could be chosen for construction when the initial water content of loess soil is equal to or less than 14%. However, when the water content is higher than 14%, if 0.5 m is still used as the pile spacing, water would not be absorbed completely and also the soil would not reach the required dry density after treatment. The existing model (equations (1) and (2)) seems a more conservative design, and it can meet the dry density requirement but still wastes quicklime and time.

From the discussion about Figure 2, if the triangular arrangement is recommended to this construction, the pile spacing coefficient would be 3.02 and the pile spacing would be 0.54 m; this means 3% less quicklime would have been used than that in the square arrangement. So it is recommended taking the triangular arrangement as the first option in the design of foundation engineering.

5. Conclusions

This paper proposes mathematical models of the center-to-center spacing of quicklime piles, considering the influence of the following factors: initial water content and dry density of the loess to be treated, the installation patterns of quicklime piles, and the installation methods. The paper also presented a definition of pile spacing coefficient. Some specific conclusions can be drawn: (1) the current formulas are conservative for constructions, but more lime is required; (2) under the same conditions, the triangular arrangement is more economical than the square one; and (3) the immersing installation procedure is more economical than the boring counterpart. Finally, by analyzing the actual engineering and using the model this paper has set, it shows that the formula about the quicklime pile spacing is more economical yet yields satisfactory stabilization effect in high water content loess soils.

Data Availability

The data used to support the findings of this study are available within the article.

Additional Points

There has been a long history for foundation treatment by quicklime pile, but as for establishing a more precise model formula used by actual construction, further research is needed to be done at present.

Loess is an aeolian silt sediment with variable amounts of sand and clay and is vulnerable to collapse in case of water immersion. By far, many approaches have been introduced to investigate the roots of loess collapsing. And the results show the microstructure of loess is the main cause leading to its collapsibility. So many methods concerning improving the collapsibility of loess have been proposed based on physical and chemical theory on increasing engineering properties of loess.

This article summarizes recent progress on the cause of loess collapsibility of loess and its improving approaches.

Conflicts of Interest

The authors declare that they have no conflicts of interest in this work.

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