Azimuthal anisotropy of $\pi^0$ and $\eta$ mesons in Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV

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The azimuthal anisotropy coefficients $v_2$ and $v_4$ of $\pi^0$ and $\eta$ mesons are measured in Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV as a function of transverse momentum $p_T$ (1–14 GeV/c) and centrality. The extracted $v_2$ coefficients are found to be consistent between the two meson species over the measured $p_T$ range. The ratio of $v_4/v_2$ for $\pi^0$ mesons is found to be independent of $p_T$ for 1–9 GeV/c, implying a lack of sensitivity of the ratio to the change of underlying physics with $p_T$. Furthermore, the ratio of $v_4/v_2$ is systematically larger in central collisions, which may reflect the combined effects of fluctuations in the initial collision geometry and finite viscosity in the evolving medium.

PACS numbers: 25.75.Dw

I. INTRODUCTION

A novel form of nuclear matter, where quarks and gluons are deconfined yet interact strongly with each other, is produced in heavy ion collisions at the relativistic heavy ion collider (RHIC) [1–4] and the large hadron collider (LHC) [5]. The hydrodynamic expansion of this matter, as well as its interactions with hard scattered partons, result in the anisotropic emission of hadrons [6, 7]. Measurements of azimuthal anisotropy for particle production provide valuable information on the transport properties of the matter [8–10].

The magnitude of the anisotropy can be studied from the azimuthal angle ($\phi$) distribution of particles relative to the second order¹ event plane (EP) angle ($\Phi$) accumulated over many events [11, 12]:

$$\frac{dN}{d\Delta \phi} \propto 1 + 2 \sum_{k=1}^{\infty} v_{2k} \cos(2k\Delta \phi);$$  \hspace{1cm} (1)

where $\Delta \phi = (\phi - \Phi)$ and $v_{2k}$ are even-order Fourier coefficients, which generally are nonzero around the elliptic flow EP [11]. In the event-plane method, an estimated EP angle $\Psi$ is determined from the particles in the event. Due to the finite number of particles used to determine $\Psi$, the $\Psi$ angle is an approximation of the true EP angle $\Phi$. The coefficient $v_{2k}$ is measured by correlating particles with $\Psi$ to obtain the raw values $v_{2k}^{obs} = \langle \cos(2k[\phi - \Psi]) \rangle$, which are then corrected by a resolution factor ($\text{Res}(2k\Psi)$) that accounts for the spread of $\Psi$ about $\Phi$ [11]:

$$v_{2k} = \frac{v_{2k}^{obs}}{\text{Res}(2k\Psi)} = \frac{\langle \cos(2k[\phi - \Psi]) \rangle}{\langle \cos(2k[\Psi - \Phi]) \rangle} \quad k = 1, 2. $$  \hspace{1cm} (2)

To minimize the nonflow biases from dijets, the particles used to estimate $\Psi$ are selected in a pseudorapidity range that is well separated (typically one unit or more) from the particles used to evaluate $v_{2k}^{obs}$ [13].

Recently, experiments at RHIC and LHC have measured significant $v_{2k}$ values for $k = 1–3$ for various particle species and over a broad range in $p_T$ [14–18]. For particles with low transverse momenta ($p_T \lesssim 3$ GeV/c), the coefficients are understood in terms of pressure-driven flow in an initial “almond-shaped” collision zone produced in noncentral collisions [19]. For higher transverse momenta ($p_T \gtrsim 6–10$ GeV/c), the anisotropy reflected by the $v_{2k}$ coefficients can be attributed to jet quenching [20] – the process by which hard scattered partons interact and lose energy in the hot and dense medium prior to fragmenting into hadrons. This energy loss manifests as a suppression of hadron yields [21], which depends on the average path-length that partons propagate through the medium [22, 23], and $v_2$ for example stems from the fact that the partons traveling in a direction parallel to the $\Phi$ angle are less suppressed than those traveling in the direction perpendicular to the $\Phi$ angle [7].

The present work exploits various PHENIX detector subsystems with a broad range in pseudorapidity for the EP determination, and provides detailed differential measurements of $v_2$ and $v_4$ for $\pi^0$ mesons and $v_2$ for $\eta$.  

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⁴ The $v_4$ coefficient can be measured with respect to the second order event plane or the fourth order event plane. In the analysis presented in this work, all $v_4$ coefficients are measured with respect to the second order event plane.
mesons in \(\sqrt{s_{NN}} = 200\) GeV Au+Au collisions. The \(v_2\) and \(v_4\) measurements for \(\pi^0\) mesons extend our earlier work \([22, 23]\). The \(v_2\) measurements for \(\eta\) mesons probe the particle species dependence of jet-quenching and test the consistency of the data with medium-induced partonic energy loss prior to vacuum hadronization \([17, 24]\). In this vacuum hadronization picture, high \(p_T\) \(\pi^0\) and \(\eta\) mesons are thought to arise from fragmentation of energetic partons after they lose energy in the medium, and hence the two types of mesons are expected to show similar level of suppression \([25]\) and similar path-length dependence or \(v_2\). Furthermore, this analysis provides a test of the previous observed scaling relation between \(v_2\) and \(v_4\), i.e. the observation that \(v_4/v_2^2\) ratio is approximately independent of \(p_T\) \([14–16, 26]\). This analysis also allows a detailed study of the biases from dijets in the determination of the event plane.

**II. MEASUREMENT**

**A. Data set and Centrality**

The measurements are based on a Au+Au collision data set at \(\sqrt{s_{NN}} = 200\) GeV collected during the 2007 running period. The minimum bias events are selected by the beam-beam counters (BBC). The collision vertex along the beam direction, \(z\), is measured by the BBC. After an offline vertex cut of \(|z| < 30\) cm and run quality selections, a total of \(\sim 3.5 \times 10^9\) minimum bias events are obtained. Event centrality for these events are determined by the number of charged particles detected in the BBCs \([13]\). A Glauber model Monte-Carlo simulation \([27]\) that includes the responses of the BBC is used to estimate, for each centrality selection, the average number of participating nucleons \(N_{\text{part}}\).

**B. Event plane measurement**

The EP angle is estimated using several detectors installed symmetrically on both sides of the nominal collision point along the beamline: the BBC \([28]\), the muon piston calorimeters (MPC) \([29]\), and the reaction-plane detectors (RXN) \([30]\). The BBCs comprise two sets of 64 Čerenkov counter modules, located at \(z = \pm 144\) cm from the nominal collision point and measure the number of charged particles over the pseudorapidity region \(3.1 < |\eta| < 3.9\). Each MPC is equipped with PbWO\(_4\) crystal scintillator towers. The north MPC has 220 towers spanning \(3.1 < \eta < 3.9\), while the south MPC has 196 towers spanning \(-3.7 < \eta < -3.1\). The MPCs have almost the same azimuth and \(\eta\) coverage as the BBCs, but have finer granularity and detect both charged and neutral particles, and hence have better EP resolution. The RXNs are situated at \(z = \pm 40\) cm from the nominal interaction point. Each comprises 12 azimuthally segmented scintillator paddles with photomultiplier read out. They are covered with a 2 cm (3.6 radiation length) thick lead photon converter and are sensitive to both charged particles and photons. The RXNs cover the pseudorapidity range \(1.0 < |\eta| < 2.8\). They are further subdivided into an outer part (RXN\(_{\text{out}}\), \(1.0 < |\eta| < 1.5\)) and an inner part (RXN\(_{\text{in}}\), \(1.5 < |\eta| < 2.8\)).

Table I outlines the \(\eta\) acceptance of BBCs, MPCs and RXNs, as well as several combined detectors from which the EP are estimated. These combinations allow for a reliable estimate of the systematic uncertainties in this measurement. The results reported in this paper use the EP from MPC+RXN\(_{\text{in}}\) \([22]\), which provides very good resolution and minimizes the possible nonflow biases from jets and dijets \([13]\).

The resolution factor \(\text{Res}\{2k\Psi\}\) is determined using the two subevents (2SE) and three subevents (3SE) methods \([11]\), as outlined in our previous analyses \([15, 24]\). In the 2SE method, the signal of a given detector combination in Table I is divided into two subevents covering equal pseudorapidity ranges in opposite hemispheres. The resolution of each subevent is calculated directly from the correlation between the two subevents:

\[
\text{Res}\{2k\Psi^A\} = \text{Res}\{2k\Psi^B\} = \sqrt{\langle \cos(2k[\Psi^A - \Psi^B]) \rangle} \quad (3)
\]

The resolution can be expressed analytically as:

\[
\text{Res}\{2k\Psi\} = \langle \cos(2k\Delta\Psi) \rangle = \frac{\chi\sqrt{\pi}}{2}e^{-\frac{\chi^2}{2}} \left[ I_{\frac{\chi^2}{2}}(\frac{\chi^2}{2}) + I_{\frac{\chi^2}{2}}(\frac{\chi^2}{2}) \right], \quad (4)
\]

where \(I_\alpha\) are modified Bessel functions of the first kind, and the resolution parameter \(\chi \propto \sqrt{M}\) is related to the multiplicity \(M\). The resolution parameter of the full detector is determined as \(\chi = \sqrt{\chi_A + \chi_B}\), which is then used to determine \(\text{Res}\{2k\Psi\}\) via Eq. 4.

The 3SE method determines the resolution factor of a given detector from the correlations of its EP with those for two other detectors in different pseudorapidity ranges:

\[
\text{Res}\{2k\Psi^A\} = \frac{\langle \cos(2k[\Psi^A - \Psi^B]) \rangle \langle \cos(2k[\Psi^A - \Psi^C]) \rangle}{\langle \cos(2k[\Psi^B - \Psi^C]) \rangle}, \quad (5)
\]

The main advantage of the 3SE method is that for a given detector \(A\), there are many choices of detectors \(B\) and \(C\),

| Detectors | \(\eta\) range |
|-----------|---------------|
| BBC       | ±[3.1, 3.9]   |
| MPC       | [−3.7, −3.1][3.1, 3.9] |
| RXN\(_{\text{in}}\) | ±[1.5, 2.8] |
| RXN\(_{\text{out}}\) | ±[1.0, 1.5] |
| RXN(in + out) | ±[1.0, 2.8] |
| MPC + RXN\(_{\text{in}}\) | ±[1.5, 2.8], [−3.7, −3.1][3.1, 3.9] |

TABLE I. Summary of the \(\eta\) coverage for the detector combinations used for the event plane measurements.
which provide independent estimates of the resolution of \( A \). The differences between the resolution estimates for the 2SE and 3SE methods are included in the evaluation of systematic uncertainties.

The left panel of Fig. 1 summarizes the \( N_{\text{part}} \) dependence of the 2SE resolution factors for various detector combinations as indicated. The resolution factors peak around \( N_{\text{part}} \sim 180 \) (i.e. the 20%-30% centrality bin) with maximum values of 0.75 for RXN, 0.53 for MPC and 0.4 for the BBC. The resolution factors for RXN\(_{\text{in}}\) and RXN\(_{\text{out}}\) are similar and show a maximum of \( \sim 0.65 \). The resolution factors for MPC+RXN\(_{\text{in}}\) are very close to those for the full RXN. The right panel of Fig. 1 shows resolution factors for \( v_4 \) that are much smaller than those for \( v_2 \). The associated resolution factors also peak for \( N_{\text{part}} \sim 180 \), reaching maximum values of 0.45, 0.18, 0.1 and 0.4 for the full RXN, MPC, BBC and MPC+RXN\(_{\text{in}}\) respectively.

\[ \cos(2\Phi) = \frac{E_3 - E_2}{E_1 + E_2} \]

C. Measurements of \( \pi^0 \) and \( \eta \) meson anisotropy

1. Reconstruction of \( \pi^0 \) and \( \eta \) mesons

Neutral pion and \( \eta \) mesons are measured via their \( \gamma\gamma \) decay channel in the electromagnetic calorimeter (EMCal, \( |\eta| < 0.35 \)) \[31\]. The EMCal comprises the lead-scintillator and lead-glass subdetectors, covering 0.75\(\pi\) and 0.25\(\pi\) in azimuth, respectively. Photons are identified using various cuts on the shower shape observed in the EMCal, as well as by comparing the observed shapes to a template profile function measured from test beam data. The invariant mass \( m_{\gamma\gamma} \) is calculated for photon pairs, which pass an energy asymmetry cut \( \alpha = |E_3 - E_2|/(E_1 + E_2) < 0.8 \) and have a minimum separation of 8 cm between their impact points in the EMCal. The combinatorial background distribution in \( m_{\gamma\gamma} \) is estimated with the event mixing technique where the two photons are selected from different events satisfying similar global requirements such as vertex, centrality and event plane direction. The mixed-event \( m_{\gamma\gamma} \) distributions are then normalized in the sidebands of the \( \pi^0 \) and \( \eta \) peaks in the real event distributions and subtracted. A small residual background is parameterized by a first-order polynomial in the regions below and above the \( \pi^0 \) and \( \eta \) peak, and then subtracted from the \( m_{\gamma\gamma} \) distribution. The raw \( \pi^0 \) and \( \eta \) meson yields are calculated by integrating a \( \pm 2\sigma \) window in \( m_{\gamma\gamma} \) around their respective peaks. This window is varied (\( \pm 2\sigma \) vs \( \pm 3\sigma \)) to check the stability of the yield. The ratios of signal to background (S/N) for \( \pi^0 \) and \( \eta \) mesons varies strongly with \( p_T \) and centrality. The S/N value generally increases with \( p_T \) and increases from central to peripheral collisions. The values of S/N for \( \pi^0 \) and \( \eta \) mesons are given in Table II for events in 0%-20% collisions. In this analysis, the reconstruction of the \( \pi^0 \) and \( \eta \) mesons is limited to \( p_T > 1 \) GeV/c and \( p_T > 3 \) GeV/c respectively, where the yields of the two mesons can be extracted with relatively small uncertainty. Further details can be found in Ref. \[23, 32\].

\[
\frac{dN}{d\Delta\phi} = N_0[1 + 2v_{2k}\cos(2\Delta\phi) + 2v_{4k}\cos(4\Delta\phi)],
\]

where \( N_0 \) stands for the yield in the \( i^{th} \) angular bin. The two results are found to be consistent within 2% of their central values. Because of the finite bin-width in \( \Delta\phi \), the extracted \( v_{2k} \) values need to be corrected up by a smearing factor \( \sigma_{\Delta\phi} = \frac{kT}{\sin(k\delta)} \), which accounts for the finite bin width \( \delta = \pi/12 \).

The \( v_2 \) and \( v_4 \) values for this method are obtained by applying both the resolution correction (Eq. 2) and

| \( p_T \) (GeV/c) | 1  | 3  | 6  | 10 |
|------------------|----|----|----|----|
| \( \pi^0 \) S/N  | 0.01 | 0.15 | 2  | 8  |
| \( \eta \) S/N    | N/A | 0.01 | 0.1 | 1  |

TABLE II. The ratios of signal to background (S/N) for \( \pi^0 \) and \( \eta \) mesons at several \( p_T \) in 0%-20% most central collisions. The values are given for pairs integrated in a \( \pm 2\sigma \) window in \( m_{\gamma\gamma} \) around their respective peaks.
smearing correction to $v_{2}^{\text{obs}}$ and $v_{4}^{\text{obs}}$ for each centrality and $p_T$ selection. To check the sensitivity of the yield extraction on our choices of bin width in $\Delta \phi$, the $v_{2}$ and $v_{4}$ values are also calculated using 18 bins in $\Delta \phi$ for $p_T < 10$ GeV/c. The results are found to be consistent with the 6 bin results within 3% of the average of the two measurements.

3. Invariant mass method

The second method of extracting $v_{2}$ and $v_{4}$ for $\pi^0$ mesons follows the procedure outlined in Refs. [33–35]. In this method, the anisotropy of same-event or foreground (frg) pairs and mixed-events or background (bkg) pairs are determined as a function of $m_{\gamma\gamma}$, denoted as $v_{2k}^{\text{frg}}(m_{\gamma\gamma})$ and $v_{2k}^{\text{bkg}}(m_{\gamma\gamma})$, respectively. The anisotropy of foreground pairs can be expressed as the sum of the contributions from the signal pairs (sig) and the background pairs in each $m_{\gamma\gamma}$ bin:

$$N_{\text{frg}} v_{2k}^{\text{frg}} = N_{\text{sig}} v_{2k}^{\text{sig}} + N_{\text{bkg}} v_{2k}^{\text{bkg}},\quad (8)$$

$$N_{\text{frg}} = N_{\text{sig}} + N_{\text{bkg}},\quad (9)$$

which gives the expression:

$$v_{2k}^{\text{sig}}(m_{\gamma\gamma}) = \frac{v_{2k}^{\text{frg}}(m_{\gamma\gamma}) - v_{2k}^{\text{bkg}}(m_{\gamma\gamma})[1 - R(m_{\gamma\gamma})]}{R(m_{\gamma\gamma})} = \frac{v_{2k}^{\text{frg}}(m_{\gamma\gamma}) - v_{2k}^{\text{bkg}}(m_{\gamma\gamma})}{R(m_{\gamma\gamma})},\quad (10)$$

where $R = N_{\text{sig}}/(N_{\text{sig}} + N_{\text{bkg}})$ is the fraction of the total number of pairs comprising the signal.

Figure 2 illustrates the steps in calculating $v_{2k}^{\text{sig}}(m_{\gamma\gamma})$ for a given $p_T$ and centrality bin. Figure 2(a) shows the distributions of the foreground $N_{\text{frg}}(m_{\gamma\gamma})$, total background $N_{\text{bkg}}(m_{\gamma\gamma})$, and the extracted signal $N_{\text{sig}}(m_{\gamma\gamma})$. The $N_{\text{bkg}}$ is determined from mixed-events in concert with a linear parameterization of the residual background, as described earlier. Figure 2(b) shows the resulting $R(m_{\gamma\gamma})$. The signal anisotropy coefficients are calculated directly as $v_{2k}^{\text{sig}}(m_{\gamma\gamma}) = \langle \cos(2k(\phi - \Psi)) \rangle$ as a function of $m_{\gamma\gamma}$, as shown by the open circles in Figs. 2(c)-(d). They have a concave shape in the $\pi^0$ signal region, and show a minimum at the $\pi^0$ mass peak. In regions far away from the $\pi^0$ mass, the $v_{2k}^{\text{sig}}$ values vary slowly with $m_{\gamma\gamma}$, reflecting the anisotropy of the background. The concave shape is a general feature of the invariant mass method for reconstructing $v_{2}$ of decay particles [33–35]: the background photon pairs on average have a small opening angle owing to the asymmetry cut, and hence they have a larger anisotropy compared to photons from $\pi^0$ decay.

The two photons of the mixed-event pairs are chosen from an event class with similar event plane orientations, so they have a sizable anisotropy $v_{2k}^{\text{bg, mix}}(m_{\gamma\gamma})$. However, because the two events used to construct the mixed-event do not have exactly the same EP angle, $v_{2k}^{\text{bg, mix}}(m_{\gamma\gamma})$ is smaller than the $v_{2k}^{\text{bkg}}(m_{\gamma\gamma})$ by a factor that depends on the EP resolution and the bin width of the EP class used for event mixing, but is independent of $m_{\gamma\gamma}$. Hence the $v_{2k}^{\text{bkg}}(m_{\gamma\gamma})$ value is obtained by first scaling the measured $v_{2k}^{\text{frg}}(m_{\gamma\gamma})$ distribution to match the $v_{2k}^{\text{frg}}(m_{\gamma\gamma})$ in regions three standard deviations away from the $\pi^0$ peak. The resulting $v_{2k}^{\text{bkg}}(m_{\gamma\gamma})$ distributions are indicated by the small dotted symbols in Figs. 2(c)-(d). The anisotropy coefficients of the signals $v_{2k}^{\text{sig}}$ are then calculated bin-by-bin in $m_{\gamma\gamma}$ according to Eq. 10. They are shown by the solid symbols in Figs. 2(c)-(d).

Figure 2(c) shows a slight increase of $v_{2}^{\text{sig}}$ at the upper end of the $\pi^0$ peak. This increase is due to overlapping clusters, which also manifests as an excess in the Gaussian fit to the signal Figs. 2(a). Since the $v_{2}^{\text{sig}}$ measurement is dominated by the points in the vicinity of the $\pi^0$ peak, the influence of this increase on $v_{2}^{\text{sig}}$ is less than 3% of its magnitude and it is included in the systematic uncertainties.

Figures 3 and 4 compare the $v_{2}$ and $v_{4}$ values obtained from the two analysis methods. The $v_{2}$ values agree within the statistical uncertainties; the systematic deviation is less than 3%. The $v_{4}$ from the $dN/d\Delta \phi$ method is systematically larger by about 5%–10%. This is due to small residual backgrounds in the integration window in the $dN/d\Delta \phi$ method. This background also leads to larger statistical uncertainty for the $dN/d\Delta \phi$ method.
because it is evaluated separately for each angular bin, while in reality this background is correlated between these angular bins. The $dN/d\Delta\phi$ method also has an extra source of systematic uncertainty arising from the number of $\Delta\phi$ bins, which can become significant for $v_4$. Consequently, the invariant mass method is used to generate the $v_4$ and $v_4/v_2^2$ results. As a cross-check, the $\pi^0$ $v_2$ and $v_4$ results are also compared and found to be consistent with the results for identified charged pions from Ref. [15].

4. Evaluating the jet bias

This measurement assumes that the EP determination is not strongly biased by the selection of $\pi^0$ and $\eta$ mesons at midrapidity. At high $p_T$, such a bias could stem from dijets associated with the $\pi^0$ or $\eta$ mesons. The pseudorapidity spread of particles from jets containing the $\pi^0$ or $\eta$ meson is typically much smaller than the pseudorapidity gap between the EP and the EMCal. However, the large rapidity swing of the away-side jet could bring jet-associated particles into the detectors used to calculate the EP, leading to a potential bias of the $v_2$ and $v_4$ values.

In earlier studies of high momentum particles, PHENIX has estimated the magnitude of this bias by embedding PYTHIA dijet events into HIJING events modulated with the experimentally measured $v_2$ signal [13, 36]. The away-side jet was found to bias the EP determination and hence, the $v_{2k}$ signal at high $p_T$, dependent on the pseudorapidity gap. In general the bias is expected to decrease with increasing pseudorapidity gap, and should be smallest for EP determined by the MPC pseudorapidity range. In this analysis, our ability to measure the EP in different pseudorapidity ranges allows for a data-driven quantification of the pseudorapidity dependence of the jet bias, as discussed below.

Figure 5 shows the EP resolution of various detectors for events containing a high $p_T$ $\pi^0$ ($p_T > 5$ GeV/$c$). No systematic $p_T$ dependence is observed for the selections studied. Figure 6 compares the $v_2(p_T)$ values for $\pi^0$, obtained with event planes determined in the MPC ($3 < |\eta| < 4$), RXN$_{in}$ ($1.5 < |\eta| < 2.8$) and RXN$_{out}$ ($1 < |\eta| < 1.5$). At low $p_T$ ($< 5$ GeV/$c$), the $v_2$ values obtained from these event planes are comparable in more central collisions. For higher $p_T$, they deviate from each other, with larger $v_2$ for RXN$_{out}$ and smaller $v_2$ for the MPC. For peripheral collisions, the values obtained with RXN$_{out}$ are significantly higher over the full $p_T$ range. These trends are consistent with the presence of a dijet bias, which grows as the pseudorapidity gap between the EP and the $\pi^0$ or $\eta$ meson is reduced. For pseudorapidity gaps $\lesssim 1-1.5$, the dijets bias the EP angle towards the direction of the $\pi^0$, which results in a larger $v_2$ value. Apparently, this bias does not affect the resolution corrections. In summary, for the centrality range used in this analysis (0%–60%), the use of MPC+RXN$_{in}$ is suf-
FIG. 5. (Color online) Event plane resolution $\text{Res}\{2\Psi\}$ for events containing a high $p_T$ $\pi^0$. Results are plotted as a function of $p_T$ of the $\pi^0$ for several EP detectors in several centrality ranges.

FIG. 6. (Color online) Comparison of $v_2$ vs. $p_T$ for $\pi^0$ mesons obtained at several centralities with event planes determined by detectors in different pseudorapidity ranges.

FIG. 7. (Color online) The $v_2$ (left panels) and nuclear modification factor $R_{AA}$ (right panels) for $\pi^0$ and $\eta$ mesons in 0%-20% (top panels) and 20%-60% (bottom panels) centrality ranges. The $v_2$ results for $\pi^0$ mesons are identical to what was published in Ref. [22]. The $R_{AA}$ data are taken from Ref. [37] ($\pi^0$, $p_T < 5$ GeV/c), Ref. [23] ($\pi^0$, $p_T > 5$ GeV/c) and Ref. [32] (eta meson). The uncertainties of $R_{AA}$ associated with $N_{coll}$ and normalization are common between $\pi^0$ and $\eta$ mesons, and are shown as shaded boxes around unity.

5. Systematic uncertainties

The primary results of this analysis are obtained with the MPC+RXN$_{in}$ event plane. The uncertainties in the resolution factors for this event plane are obtained by comparing the values obtained for the 2SE and the 3SE methods. They are estimated to be 8% (12%) in central collisions and 4% (6%) in midcentral collisions for $\text{Res}\{2\Psi\}$ ($\text{Res}\{4\Psi\}$). These uncertainties allow all points to move up and down by the same multiplicative factor.

The systematic uncertainties for $v_2^{\text{obs}}$ and $v_4^{\text{obs}}$ are estimated by varying the identification cuts for $\pi^0$ and $\eta$ mesons, the parameterization of the residual background and the peak integration window in the $m_{\gamma\gamma}$ distributions. These uncertainties are correlated in $p_T$ and are added in quadrature to give the total systematic uncertainties. For the $\pi^0$ analysis, these uncertainties are estimated to be 10% (15%) in central collisions and 3% (5%) in midcentral collisions for $v_2^{\text{obs}}$ ($v_4^{\text{obs}}$). For the $\eta$ meson analysis, the uncertainties are significantly larger primarily because of the lower signal-to-background ratio. These uncertainties are estimated to be 15% in central collisions and $\sim$ 10% at other centralities.
and Fig. 32 shows that significant systematic uncertainties.

The shaded boxes represent the indicated centrality selections. These patterns complement our earlier suppression measurements \[23, 32\] (reproduced in the right panel of Fig. 7), which show the same suppression patterns for \(\pi^0\) and \(\eta\) mesons. These results are in agreement with the expectations for in-medium energy loss of parent partons prior to their fragmentation into hadrons in the \(p_T\) region where jet quenching is expected to be dominant mechanism \((p_T > 4 \text{–} 5 \text{ GeV/c}).\)

The transition from anisotropy driven by hydrodynamic flow to anisotropy driven by jet quenching can be probed by the ratio \(v_4/v_2\). Perfect fluid hydrodynamics predicts a value of 0.5 for this ratio \[38\]. However, geometrical fluctuations and other dynamical fluctuations, as well as viscous damping, can significantly increase the magnitude of this ratio, especially in central collisions \[26, 39\]. Furthermore, the directions that maximize collective flow and jet quenching may not be the same \[40, 41\]. Hence, this ratio could change in the \(p_T\) region where jet quenching begins to dominate.

The results of \(v_4(p_T)\) and the \(v_4/v_2^2\) ratio for \(\pi^0\) in several centrality ranges are shown in Fig. 8 and Fig. 9, respectively. Results are also combined into a wide centrality range (20%–60%) for better statistical precision. Figure 8 shows that significant \(v_4\) values are observed even for \(p_T > 5 \text{ GeV/c.}\) The \(v_4/v_2^2\) ratios shown in Fig. 9 are approximately independent of \(p_T\), with values of \(\sim 1.0\) and \(\sim 0.8\) for the 0%–20% and the 20%–40% and 40%–60% centrality selections respectively. This pattern at low \(p_T\) \((p_T \lesssim 5 \text{ GeV/c})\) is consistent with our prior observations of this ratio for inclusive charged hadron measurements \[15\]. On the other hand, possible variations of this ratio at higher \(p_T\) could be masked, owing to the limited statistics of this measurement. The deviation of the \(v_4/v_2^2\) value from the expectation of ideal hydrodynamics and the increase of this ratio from midcentral to more central collisions may reflect the combined effects of fluctuations in the initial geometry and finite viscosity in the evolving medium \[39\].

**III. RESULTS AND DISCUSSION**

The primary results of this analysis are obtained with MPC+RXN\textsubscript{m} event plane. The left panels of Fig. 7 compare the \(v_2\) for \(\pi^0\) and \(\eta\) mesons for \(p_T > 4 \text{ GeV/c,}\) both obtained with the \(dN/d\Delta \phi\) method for two centrality ranges. Within uncertainties, the magnitude of the \(v_2\) values for both particle species are the same for the measured \(p_T\) range. This agreement indicates that the differences between their masses \([m_\eta = 0.548 \text{ GeV, m}_{\pi^0} = 0.135 \text{ GeV}]\) and quark content \([(u\bar{u} + d\bar{d})/\sqrt{2}\) for \(\pi^0\) and \((u\bar{u} + d\bar{d} - 2s\bar{s})/\sqrt{6}\) for \(\eta\) in the SU(3) limit] do not lead to appreciable differences in the \(\pi^0\) and \(\eta\) meson \(v_2\) values for the centrality ranges studied. A clear decrease of \(v_2\) with \(p_T\) is also evident, especially for the 20%–60% centrality selection. These patterns complement our earlier suppression measurements \[23, 32\] (reproduced in the right panel of Fig. 7), which show the same suppression patterns for \(\pi^0\) and \(\eta\) mesons. These results are in agreement with the expectations for in-medium energy loss of parent partons prior to their fragmentation into hadrons.

**IV. SUMMARY AND CONCLUSIONS**

PHENIX has measured the azimuthal anisotropy for \(\pi^0\) and \(\eta\) mesons in Au+Au collisions at \(\sqrt{s_{NN}} = 200 \text{ GeV}\). The anisotropy coefficients \(v_2\) and \(v_4\) are measured with event planes determined in forward detectors, which enable a minimum pseudorapidity gap of 1.2 units between the event plane and the \(\pi^0\) or \(\eta\) mesons. This pseudorapidity gap is found to greatly reduce auto-correlation biases due to dijets over the 0%–60% centrality range. The magnitude of the \(v_2\) values extracted for \(\pi^0\) and \(\eta\) mesons, over the common \(p_T\) range of 3–14 GeV/c, are observed to be similar, suggesting in-medium energy loss of parent partons prior to their fragmentation into.
hadrons. The $v_4$ values for $\pi^0$ mesons are found to be significantly above zero for the measured $p_T$ range of 1–9 GeV/c. The $v_2/v_4^2$ ratios are independent of $p_T$ with a magnitude between $\sim 0.8$ and $\sim 1.0$ depending on the centrality range, which may reflect the combined effects of fluctuations in the initial collision geometry and finite viscosity in the evolving medium.

ACKNOWLEDGMENTS

We thank the staff of the Collider-Accelerator and Physics Departments at Brookhaven National Laboratory and the staff of the other PHENIX participating institutions for their vital contributions. We acknowledge support from the Office of Nuclear Physics in the Office of Science of the Department of Energy, the National Science Foundation, Abilene Christian University Research Council, Research Foundation of SUNY, and Dean of the College of Arts and Sciences, Vanderbilt University (U.S.A), Ministry of Education, Culture, Sports, Science, and Technology and the Japan Society for the Promotion of Science (Japan), Conselho Nacional de Desenvolvimento Científico e Tecnológico and Fundação de Amparo à Pesquisa do Estado de São Paulo (Brazil), Natural Science Foundation of China (P. R. China), Ministry of Education, Youth and Sports (Czech Republic), Centre National de la Recherche Scientifique, Commissariat à l’Énergie Atomique, and Institut National de Physique Nucléaire et de Physique des Particules (France), Bundesministerium für Bildung und Forschung, Deutscher Akademischer Austausch Dienst, and Alexander von Humboldt Stiftung (Germany), Hungarian National Science Fund, OTKA (Hungary), Department of Atomic Energy and Department of Science and Technology (India), Israel Science Foundation (Israel), National Research Foundation and WCU program of the Ministry Education Science and Technology (Korea), Physics Department, Lahore University of Management Sciences (Pakistan), Ministry of Education and Science, Russian Academy of Sciences, Federal Agency of Atomic Energy (Russia), VR and Wallenberg Foundation (Sweden), the U.S. Civilian Research and Development Foundation for the Independent States of the Former Soviet Union, the US-Hungarian Fulbright Foundation for Educational Exchange, and the US-Israel Binational Science Foundation.

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