Three-Dimensional High Spatial Localization of Efficient Resonant Energy Transfer from Laser-Assisted Precipitated Silver Clusters to Trivalent Europium Ions

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Abstract: We report on the 3D precipitation, using a direct laser writing approach, of highly fluorescent silver clusters in a Eu³⁺-doped silver-containing zinc phosphate glass. Micro-spectroscopy of fluorescence emission shows the ability to continuously adjust the local tri-chromatic coordinates in the CIE (Commission Internationale de l’Éclairage) chromaticity diagram between red and white colors, thanks to the laser-deposited dose and resulting tunable combination of emissions from Eu³⁺ and silver clusters. Moreover, continuous-wave and time-resolved FAST-FLIM spectroscopies showed a significant enhancement of the fluorescence emission of Eu³⁺ ions while being co-located with UV-excited laser-inscribed silver clusters. These results demonstrate the ability to perform efficient resonant non-radiative energy transfer from excited silver clusters to Eu³⁺, allowing such energy transfer to be highly localized on demand thanks to laser inscription. Such results open the route to 3D printing of the rare earth ions emission in glass.

Keywords: silver clusters; rare earth ions; femtosecond laser inscription; FLIM spectroscopy; resonant transfers; Dexter process; FRET process; CIE chromaticity diagram

1. Introduction

Photonics has been clearly identified as a key enabling technology. The development of such penetrating technology relies on its ability to integrate and miniaturize components and devices. Therefore, the development of innovative materials together with the fabrication processes remain a central issue. Glass materials have shown, thanks to the development of fiber technology, for instance, that they are excellent candidates for optical applications. New solutions should be found for the enhancement and promotion of 3D architectures. This requires developing intense local physical effects that could be structured in 3D. Direct laser writing offers numerous solutions for shaping and inscribing functionality in glass [1]. Moreover, designed glass compositions can offer additional possibility for implementing multiple functionalities, such as luminescence, for instance [2]. Structuring efficient emissions in various spectral range remains an important challenge. This last decade, we demonstrated that femtosecond direct laser writing (DLW) in a high optical quality photosensitive silver-containing zinc phosphate glass allows for implementing a 3D fluorescent structure formed by the aggregation of silver ions and silver atoms within the glass volume [3], which could be a solution for perennial three-dimension high-density
data storage [4–7]. The cluster exhibits a broad excitation spectrum from 280 nm up to at least 550 nm. This local precipitation of silver clusters is preceded by the localized creation of a space charge separation at the root of a perennial high-amplitude (\(\sim 10^{8–9} \, \text{V/m}\)) static electric field, leading to the local breaking of centrosymmetry and thus allowing for an efficient electric field-induced second-harmonic generation (\(\chi^{(2)}_{\text{eff}} \sim 0.8 \, \text{pm/V}\)) [8,9]. Moreover, the spatial structuring of the incident laser beam led us to achieve the first demonstration of bulk structuring by means of optical vortex-induced DLW [10], locally producing correlative optical contrast in terms of silver cluster fluorescence, and of effective second-order nonlinear optical properties. Despite the high repetition rate of the laser/glass interaction to produce the silver clusters, the associated irradiation regime is indeed an athermal regime for which energy deposition at the voxel interaction is very moderate [11,12]. This results in a very limited local temperature increase (100 °C or less) so that temperature remains much below the glass transition temperature in the specific irradiation regime that leads to silver cluster creation [11,12]. Finally, these innovative laser-induced multi-scale structures were tuned into silver metallic nano-crystallites by means of thermal annealing, creating a composite metal-dielectric material with plasmonic properties [13]. The local formation of various types of molecular silver clusters (labeled Ag\(_{m}^{n+}\), such as in ref [13]) by DLW was recently shown to be partially or fully inhibited by original dual-color DLW with the co-illumination of a CW UV beam with the fs IR structuring beam, opening interesting potentials in terms of super-resolution DLW [14]. The co-doping of glasses with both rare earth ions and noble metal ions has been increasingly reported [15–18] for optoelectronic devices such as white light emitting diodes, three-dimensional displays, and solar cells [15,17–20]. Indeed, efficient energy transfer between silver species and europium ions was described and achieved in various materials such as glasses and zeolite materials [15,16,21–26]. In glasses, in addition to the traditional melt technique to incorporate silver species with rare ions, different methods of preparation have been described, such as the ion-exchange processes. The modification of the quantum yield of fluorescence emission has been described thanks to the presence of silver clusters and silver nanoparticles [15]. An enhancement of the rare earth emission by energy transfer from silver clusters to Eu\(^{3+}\) ions has been observed in various matrices, such as in silicate [22,23] or borate [27].

In most of the investigations, there was no control of the spatial distribution of the rare earth ions’ emissions and the 3D organization of the luminescent structure was not considered. In the specific case of photonic integrated circuits, the issue of the 3D organization of robust luminescent structure is crucial. The goal is thus not solely the efficiency of the luminescent structure, but also the engineering of a luminescent 3D photonic structure. It requires one to be able to foster locally efficient transfer or enhancement mechanisms between noble ion-based aggregates and rare earth ions, for instance between silver species and europium ions.

In this article, we report on the co-doping of a silver-doped zinc phosphate glass with europium Eu\(^{3+}\) rare earth ions and the 3D structure of the luminescent properties. The absorption, excitation, and emission properties of the pristine co-doped glasses are investigated, and micro-luminescence properties are characterized after femtosecond laser direct writing and the local precipitation of fluorescent silver clusters. The origin of the interaction between the silver clusters and the europium ions is investigated in order to elucidate the potential contributions of radiative and non-radiative transfers. A local field enhancement effect due to hypothetical formation of metallic nanoparticles is also discussed.

2. Experimental Section

2.1. Glass Synthesis and Sample Preparation

The europium-doped silver-containing zinc phosphate glass with the composition 99.2[54.1 PO\(_3\)\(_2\)/37 ZnO/1.4 GaO\(_3\)/2/7.5 AgO\(_1\)/2] – 0.8 Eu\(_2\)O\(_3\) (mol. %) was prepared using classical melt/quench technique using platinum crucible. After annealing at 30 °C below the glass transition temperature, the glass is cut to 1 mm thick sample with typically
1 cm lateral dimensions and polished to optical quality. Hereafter, the co-doped glass sample is referred to as PZnAg:Eu. For nanoparticle development effect investigation, the glass was heat-treated at 400 °C, typically 20 °C above the glass transition temperature, for 30 min.

2.2. Transmission, Excitation and Emission Spectroscopies

The transmission spectroscopy was performed with a Carry 500 (differential transmission spectrometer from Varian (Agilent, Santa Clara, CA, USA) from 250 to 800 nm. The excitation and emission spectroscopies were performed with a SPEX Jobin Yvon fluorescence spectrometer equipped with double monochromator and Peltier cooled PMT (Horiba Jobin Yvon GmbH, Haching, Germany).

2.3. Femtosecond Direct Laser Writing

DLW was performed using a Ytterbium fs oscillator (T-pulse 200, 9.1 MHz, 390 fs at 1030 nm, Amplitude Systèmes, Pessac, France), focused with a microscope objective (M Plan Apo NIR, 20 × NA 0.4, Mitutoyo, Kawasaki, Japan). The transmitted irradiances were controlled by an acousto-optic modulator, enabling focused energies up to 100 nJ and associated focused irradiances up to 20 TW/cm². The positioning and displacement of the sample were performed with a high-precision 3D translation stage (XMS-50 stages, Micro-Contrôle Spectra Physics, Beaune-la-Rolande, France). A laser–matter interaction matrix was performed, by producing 18 structured squares, each composed of 10 lines of 100 µm spaced by 10 µm, associated to 6 irradiances spanning from 2 to 6.7 TW/cm², and 3 translation speeds of 10, 50 and 100 µm/s, respectively, corresponding to the local accumulation of $3.1 \times 10^6$, $6.2 \times 10^6$, and $3.1 \times 10^5$ pulses.

2.4. Absorption Micro-Spectroscopy of the Structured Sample

Transmission measurements were performed in bright-field using a ‘CRAIC Technologies’ microscope equipped with a Xenon lamp and a condenser as a white light source and with a spectrometer equipped with CCD. A conjugated 10× magnification microscope objective was used to collect the transmitted light through the laser-induced structures. For such micro-transmission measurements, the reference spectrum was recorded through the pristine glass, exactly in the same geometrical conditions for the measurement through the laser-induced structures, which excludes any artifacts from distinct collection issues. As a consequence, the resulting transmission measurements gave direct experimental access to the local differential micro-extinction due to the laser-induced structures. Such a local differential micro-extinction, interpreted in terms of a linear absorption coefficient, is a spatially averaged value over a $50 \times 50$ µm² surface, successively overlapping each of the $100 \times 100$ µm² laser-induced structures.

2.5. Fluorescence Micro-Spectroscopy of the Structured Sample

Fluorescence spectrum measurements were performed in an epi-collection scheme, with a high spectral resolution micro-spectrometer (LabRAM HR800 from Jobin-Yvon, (Horiba Jobin Yvon GmbH, Haching, Germany) with 150 grooves/cm grating for the spectral dispersion of the fluorescence in the near-UV and visible region) for three different conditions. First, a 325 nm excitation with a UV He-Cd laser source (30 mW, TEM 00, Kimmon, Tokyo, Japan) was focused with a UV-enhanced Cassegrain objective (36 × NA 0.5), and fluorescence was collected over the range of 330–750 nm. Second, a 405 nm excitation with a near-UV laser diode (100 mW, TEM00, OBIS from COHERENT, Santa Clara, CA, USA) was focused with an Olympus refractive objective (100 × NA 0.9), and fluorescence was collected over the range of 450–750 nm. Finally, a 532 nm excitation with a laser diode (100 mW, TEM00, monomode, Coherent, Santa Clara, CA, USA) was focused with the same Olympus refractive objective (100 × NA 0.9), and fluorescence was collected over the range of 550–750 nm. Great care was taken to provide spectrally corrected fluorescence spectra for each of the three conditions.
2.6. Time-Resolved Fluorescence Micro-Spectroscopy of the Structured Sample

The fluorescence lifetime imaging microscopy (FLIM) analysis was performed with a Picoquant MT200 microscope equipped with two MPD single photon avalanche diodes (SPADs) and a PicoHarp300 timing board for time-correlated single photon counting (TCSPC) operation. The pulsed laser source was a frequency-doubled 6 ps coherent MIRA 900 laser, tuned at 435 nm, with a repetition rate set to 4.75 MHz via an acousto-optic pulse picker. The laser was reflected to a 100 × 1.40 NA objective (UPLSAP0100XO, Olympus, Tokyo, Japan) by an 80%T/20%R spectrally flat beam splitter, and the fluorescence was collected by the same objective and transmitted by the same beam splitter to the confocal optics and detector after excitation light was rejected by a band-pass filter (HQ510/80 with a 470–550 nm transmitted spectral window, Chroma Technologies, Rockingham, VT, USA). The laser was scanned by means of a piezoelectric stage in a grid pattern of 156 nm steps and 0.6 ms/pixel. The shown FLIM images were calculated using the so-called “FAST-FLIM” algorithm, where for each pixel, the reported lifetime was calculated as the first statistical momentum of the histogram distribution of the single photon arrival times, minus a reference time taken at the onset of the decay curve. Note that the shown FLIM images include both temporal and intensity information of the collected fluorescence, as the color code depicts the FAST-FLIM average arrival times on the one hand and the brightness levels depicts the number of collected events on the other hand. Alternatively, curve fitting with a multi-exponential model was performed on decays with better statistics, corresponding to the binning of pixels of larger regions of interest. In the latter case, tail fitting could be applied thanks to the shortness of the instrumental response function (about 40 ps FWHM).

3. Results and Discussion
3.1. Photoluminescence in Bulk Glass

The absorption spectrum in the range 250–800 nm obtained for the PZnAg-Eu glass is shown in Figure 1. The UV edge is around 270 nm mainly due to silver ions absorption as previously observed for silver ions containing zinc phosphate glass [28]. Additional characteristic absorption bands of Eu³⁺ ions are observed at 318, 362, 380, 393, 464 and 526 nm assigned to the transition from the ground state ⁷F⁰ to excited states ⁵H₃, ⁵D₄, ⁵G₂, ⁵L₆, ⁵D₂ and ⁵D₁, respectively. There is no evidence of Eu²⁺ formation in the glasses and no absorption band above 300 nm, which could be attributed to surface plasmon resonance or silver cluster species such as (Ag₂)⁺ or (Ag₃)²⁺, for instance.

![Figure 1](image-url)

**Figure 1.** Linear absorption coefficient of the pristine PZnAg:Eu glass, mostly showing the UV cut-off due to the silver ion insertion below 300 nm, as well as the much weaker and narrow 4f–4f transition lines of the Eu³⁺ ions (see insert).
Fluorescence spectroscopy have been measured under different UV excitation wavelengths to investigate the emission properties of silver and Eu$^{3+}$ ions, and the results are shown in Figure 2a. Under 235 nm excitation, two broad emission bands are observed due to two different intrinsic environments of silver with peak emission at 290 (site A) and 380 nm (site B), as well as the characteristic emissions of the 4f–4f transitions of Eu$^{3+}$: $^5D_{0} \rightarrow ^7F_{j}$ ($j = 0–6$). The site A emission is assigned to Ag$^+$ ions with the $^3D_{j} \rightarrow ^1S_{0}$ transition, while site B emission is assigned to (Ag$^+$)$_2$ pairs with the $^3S_{1} \rightarrow ^3S_{0}$ transition [29]. Note that the considered silver ion concentration makes site B largely preponderant compared to site A [2]. Note also that emission spectra of Figure 2a emitted with the present PZnAg:Eu glass are highly similar to that reported for a very close composition of PZnAg (without Europium insertion) in Figure 2 from Petit et al. [2]: this makes us confident that there is no significant existence of broadband Eu$^{2+}$ emission in the visible range in the present paper in the pristine glass (nor in the laser-induced modifications). With the increase in the excitation wavelength to 260 nm, almost exclusively site B emission as well as the characteristic emission of Eu$^{3+}$ are observed. Excitation at UV light about 235 nm or 260 nm, promotes the electron to the excited state of both sites A and B, or site B, respectively. Thus, the excited electrons can relax to the ground state radiatively, but also non-radiatively, including relaxation paths involving energy transfers to the neighboring Eu$^{3+}$ ions. The occurrence of energy transfer from silver sites to Eu$^{3+}$ ions is favored by the energy level accordance between the excited states of the silver sites with the $^5L_{6}$ level of Eu$^{3+}$ ions. Under excitation at 365 nm, only the line-shape characteristics emissions of the Eu$^{3+}$ transitions at 578, 590, 612, 652, and 702 nm, corresponding to the Eu$^{3+}$ ions emission $^5D_{0} \rightarrow ^7F_{j}$ ($j = 0–4$), are observed.

![Fluorescence emission spectroscopy](image)

**Figure 2.** (a) Fluorescence emission spectroscopy of the pristine PZnAg:Eu sample for three distinct excitation wavelengths, showing two broad emission bands of two distinct environments of the silvers ions, labeled site A (exc. 235 nm and em. 290 nm, lower amplitude) and site B (exc. 260 nm and em. 380 nm, larger amplitude), as well as the emission of the 4f–4f transitions from the $^5D_{0}$ level of the Eu$^{3+}$ ions (left). Note that the excitation at 365 nm is selective of the Eu$^{3+}$ excitation, compared to the excitation of the Ag$^+$ ions. (b) International Commission on Illumination (CIE) chromaticity diagram of the pristine PZnAg:Eu sample for three distinct excitation wavelengths.

Based on the photoluminescence spectra of the glasses presented in Figure 2, the colors of samples under the three distinct excitations at 235, 260, and 365 nm were characterized by International Commission on Illumination (CIE) chromaticity diagram (Figure 2b). The colors shift from purplish pink to red with the increase in excitation wavelength from 235 to 365 nm, which demonstrates that the luminescence color can be systematically tuned by changing the excitation wavelength.

The photoluminescence excitation spectra are shown in Figure 3. By monitoring the emission at 290 nm (site A), a broad excitation band centered at 230 nm is observed, attributed to Ag$^+$ ion. At 340 nm (site B), two overlapping broad excitation bands are observed, centered at 230 and 260 nm, from the Ag$^+$ ion and (Ag$^+$)$_2$ pairs, respectively. When monitoring the Eu$^{3+}$ emissions at 612 or 700 nm, besides the two broad excitation
bands of silver originating from the energy transfer of Ag\(^+\) ions and (Ag\(^+\))\(_2\) pairs energy transfer to the rare earth ions, several characteristic f–f transitions’ sharp lines are observed. Under UV light, Ag\(^+\) ions and (Ag\(^+\))\(_2\) pairs can be excited to the \(^3\)D\(_j\) and \(S\)\(_i\) energy levels, respectively, and then the non-radiative \(S\)\(_1\)→\(S\)\(_0\) and \(^3\)D\(_j\)→\(S\)\(_0\) transitions may transfer the excitation energy non-radiatively to Eu\(^{3+}\) ions, with such populated Eu\(^{3+}\) excited levels leading then to the observed typical Eu\(^{3+}\) fluorescent emission. Such non-radiative energy transfer is understood as a non-radiative resonant relaxation from the silver species (donor) to the Eu\(^{3+}\) ions (acceptor), without any electron transfer. Indeed, the overlapping of excitation bands evidences the potential ability of energy transfer from silver ionic species to the Eu\(^{3+}\) ions. Furthermore, no fluorescence emission signature of Eu\(^{2+}\) ions was observed, which corroborates the absence of electron transfer in the present energy transfer.

![Fluorescence excitation spectra of the pristine PZnAg:Eu sample for three distinct wavelengths](image-url)

**Figure 3.** Fluorescence excitation spectroscopy of the pristine PZnAg:Eu sample for three distinct emission wavelengths, showing two broad excitation bands of two distinct environments of the silvers ions, labeled site A (exc. 235 nm and em. 290 nm) and site B (exc. 260 nm and em. 380 nm), as well as the excitation of the 4f–4f transitions of the Eu\(^{3+}\) ions.

### 3.2. Direct Laser Writing of Fluorescence Structures

Figure 4a shows a wide-field fluorescence microscopy image of coil patterns obtained by DLW for PZnAg:Eu glass sample motion with controlled speed from 10 to 100 \(\mu\)m/s (corresponding to C, B and A lines), and for different irradiances from 4.0 to 6.7 TW cm\(^{-2}\) (labeled columns 3, 4, 5 and 6). These patterns allow for investigating the influence of the laser parameters in the silver clusters growth and their interaction with the Eu\(^{3+}\) ions. A high-resolution confocal image for excitation 435 nm (obj. 100× NA1.4) is given in Figure 4b, showing the detailed distribution of the fluorescent double-line structure produced by several laser passes. These double lines correspond to the formation of parallel planes containing the silver clusters at the border of the voxel of interaction. This phenomenon has been described in detail elsewhere [4].
Figure 4. Laser–matter interaction matrix: (a) wide-field fluorescence microscopy (Objective (obj.) 20× NA0.4, excitation at 375 nm), revealing the laser-induced fluorescence of the 100 × 100 µm² patterns after DLW; (b) confocal microscopy imaging (oil obj. 100× NA1.4, excitation 435 nm, collection from 470 to 550 nm), zooming in on part of the pattern C3 (10 µm/s, 4 TW/cm²), revealing in detail the laser-induced fluorescence of the 100 × 100 µm² surface giving a direct experimental access to the local differential micro-absorption due to the laser-induced structures. They are presented in Figure 5a,b for speeds of 10 and 100 µm/s, respectively. These spectra were decomposed by Gaussian contributions. Two contributions are observed around 335 nm (3.7 eV) and around 285 nm (4.35 eV). These two contributions increase in intensity with the irradiance and decrease in intensity with the speed. As can be seen, the relative intensity of these two bands is modulated by the dose deposition indicating that several centers are formed during the DLW process. The strongest dose tends to favor the absorption band around 335 nm (3.7 eV).

Micro-absorptions measurements were performed in transmission mode both in a pristine area of the glass and in structures zones over a 50 × 50 µm² surface giving a direct experimental access to the local differential micro-absorption due to the laser-induced structures. They are presented in Figure 5a,b for speeds of 10 and 100 µm/s, respectively. These spectra were decomposed by Gaussian contributions. Two contributions are observed around 335 nm (3.7 eV) and around 285 nm (4.35 eV). These two contributions increase in intensity with the irradiance and decrease in intensity with the speed. As can be seen, the relative intensity of these two bands is modulated by the dose deposition indicating that several centers are formed during the DLW process. The strongest dose tends to favor the absorption band around 335 nm (3.7 eV).

Figure 5. Micro-absorption spectroscopy of the laser–matter interaction matrix for laser-induced squares, observed with a 50 × 50 µm² field of view, showing the spatially averaged differential linear absorption coefficient with respect to the pristine glass, revealing the creation and growth of two mains absorption bands (typically centered at 335 (3.7 eV) and 285 nm (4.35 eV), depending on irradiation conditions) with respect to the laser irradiance at constant speed translations of (a) 10 and (b) 100 µm·s⁻¹. Note that the differential effective linear absorption coefficient results from the laser-structured pattern transmission with respect to that of the pristine glass, so that the differential effective linear absorption coefficient corresponds to the additional absorption coefficient resulting from the laser-induced modifications: the differential effective linear absorption coefficient of the pristine glass is thus 0 cm⁻¹ over the full spectrum, by definition.

The micro-emission spectroscopy of laser-induced silver clusters are presented in Figure 6 for two different excitations wavelengths at 325 and 405 nm as a function of the
sample motion velocity for 6.75 TW.cm⁻² irradiance (Figure 6a,c) and as a function of the irradiance for a fixed sample motion velocity of 10 µm/s (Figure 6b,d).

![Fluorescence Intensity Graphs](image)

**Figure 6.** Micro-emission fluorescence spectroscopy of the laser/matter interaction matrix for some laser-induced squares. Excitation at 325 nm (reflective obj. 36×, NA 0.4): (a) dependence on sample translation velocity (irradiance = 6.7 TW/cm²), and (b) dependence on irradiance (translation velocity = 10 µm/s). Excitation at 405 nm (refractive obj. 100×, NA 0.9): (c) dependence on sample translation velocity (irradiance = 6.7 TW/cm²), and (d) dependence on irradiance (translation velocity = 10 µm/s).

At 325 nm (Figure 6a,b), the emission spectra consist of two major contributions: one broad emission ranging from 400 to 700 nm attributed to silver nanoclusters and sharp emission peaks within the 575 to 715 nm region assigned to Europium ions. The decrease in sample velocity (Figure 6a) and the increase in the irradiance (Figure 6d) corresponding to a rise in the deposited dose promote the increase in the broad emission band intensity assigned to the formation of Ag₈cm⁺⁺ species and also promote the emission of the europium ions. The most intense emission of Eu³⁺ around 612 nm is attributed to the hypersensitive electric dipole transition (⁵D₀→⁷F₂). This emission is strongly influenced by the chemical environment of the Eu³⁺ ions in the host network. On the other hand, the ⁵D₀→⁷F₁ transition occurs via the magnetic dipole mechanism and its intensity is not sensitive to the chemical environment of Eu³⁺ ions. Therefore, the emission intensity ratio of these two transitions can be used to highlight a site evolution of the rare earth ion. In the present case, one can notice that the spectral shape of the 4f→4f transition remains constant and the intensity ratio between the ⁵D₀→⁷F₂ and ⁵D₀→⁷F₁ also remains at a constant value of 4.1 ± 0.1. Thus, an absence of major modification of the chemical environment at the vicinity of the Eu³⁺ after DLW can be assumed.

Micro-fluorescence emission spectra demonstrate interesting behavior in terms of display and colorimetry. Indeed, the fluorescence emission analysis under UV excitation at 325 nm and associated projection in the XYZ tri-chromatic coordinates in the CIE chromaticity diagram shows that the chromatic coordinates can be continuously controlled in 3D by means of laser irradiation, namely from red (almost pristine glass with quasi-null action of the laser inscription) to white light emission, as shown in Figure 7. In the case of the largest irradiances (I = 6.7 TW/cm² for patterns A6, B6 and C6 depicted in Figure 7a), the
trichromatic coordinates get very localized in the white emission domain whatever the three used velocities suggesting that the broadband silver cluster emission dominates the reddish contribution of Eu$^{3+}$ ions in the resulting tri-chromatic behavior. Similarly, in the case of the lowest velocity $v = 10 \mu m/s$ (namely, the largest number of cumulated pulses with patterns C3 to C6 depicted in Figure 7c), the deposited dose is also high enough to produce enough efficient fluorescent silver clusters to overcome the Eu$^{3+}$ emission and dominate the resulting tri-chromatic behavior. However, a larger velocity of 50 $\mu m/s$ tends to limit the amount of silver clusters and its fluorescence emission amplitude, locally allowing for controlling the tri-chromatic coordinates between the initial red coordinates of the pristine glass and the white light emission of the silver clusters, as shown between points B2 and B3 in Figure 7b. Such measurements result from micro-luminescence in confocal microscopy, so that they are measured at the silver cluster positions. By adjusting the probed volume of the material on the one hand, and by fixing the filling rate of silver cluster (typically with the inter-distance between successive laser passes in a given plane, or by producing thick multi-plane patterns) on the other, one can fully control the continuous evolution of the measured tri-chromatic coordinate between red to white emission. This thus suggests the ability to perform the localized 3D inscription of emitting areas with tunable tri-chromatic coordinates, which goes beyond the spatially homogeneous control of the tri-chromatic coordinates means of selecting different fluorescence excitation wavelengths, as shown in Figure 2b (from the pristine Eu$^{3+}$-based red emission to a pinkish emission resulting from the red Eu$^{3+}$ ion emission and the blue Ag$^{+}$ ion emission in the pristine glass). Laser inscription thus allows an additional experimental parameter to tune the 3D localized tri-chromatic coordinates.

To further investigate the energy transfer from silver clusters to Eu$^{3+}$ ions, time-resolved spectroscopy of silver nanocluster emission was obtained for the PZnAg and PZnAg:Eu glasses, for a collection over the 470–550 nm spectral range and using a pulsed excitation (6 ps, 4.75 MHz) at 435 nm. The collected fluorescence predominantly corresponds to that of silver clusters, because Eu$^{3+}$ ions show no emission in this spectral range and because Ag$^{+}$ ions of the glass matrix show negligible fluorescence excitation. In these conditions, Figure 8a,b show the FAST-FLIM images for the laser inscribed patterns, where the color code and the brightness depict the pixel-to-pixel FAST-FLIM average lifetime and the associated fluorescence intensity, respectively. For both the PZnAg and PZnAg:Eu glasses, the FAST-FLIM images corroborate the double-line spatial distribution of laser-induced fluorescent silver clusters, as shown in Figure 4. The intensity weighted FAST-FLIM lifetime histograms were extracted from Figure 8a,b, and are reported in Figure 8c. These histograms clearly show the mean lifetime shortening of the silver cluster excited states in the presence of Eu$^{3+}$ ions, with a typical peak value of the histograms occurring at a shorter lifetime of 1.94 ns for the PZnAg:Eu glass, compared to

![Figure 7. CIE chromaticity diagram of the laser/matter interaction matrix for some laser-induced squares with excitation at 325 nm. (a) Sample velocity dependence for the highest laser irradiance of 6.7 TW/cm$^2$; (b) laser irradiance dependence for the intermediate sample velocity of 50 $\mu m/s$; and (c) laser irradiance dependence for the lowest sample velocity of 10 $\mu m/s$.](image)
the 2.44 ns lifetime for the PZnAg glass. This supports the hypothesis of a quenching
by energy transfer from these clusters to the neighboring Eu$^{3+}$ ions which directly af-
et effects the emission rate of the cluster emission. Figure 8c also reveals a lower emission
intensity of silver clusters in the presence of Eu$^{3+}$ ions, such partial emission quenching
being also consistent with nonradiative energy transfer by resonant energy transfer from
silver clusters to Eu$^{3+}$ ions. By properly taking into account the normalization with the
incident pump intensity at 435 nm for both histograms of Figure 8c, the corresponding
time-integrated intensity of both PZnAg and PZnAg:Eu glasses led to the intensity quench-
ing $Q_{f_{\text{fluo}}}^{\text{Ag, Eu}} / f_{\text{fluo}}^{\text{Ag}} = 1 - f_{\text{fluo}}^{\text{Ag, Eu}} / f_{\text{fluo}}^{\text{Ag}} \sim 41\%$ of the silver cluster emission. Note that such
global intensity quenching includes any sources of quenching, namely the energy transfers
at play towards the Eu$^{3+}$ ions but also other possible phenomena whose contributions will
be discussed below.

Figure 8. (a) Composite image of the laser-induced pattern C3 (10 $\mu$m/s, 4 TW/cm$^2$) in the PZnAg glass depicting a color
image of the laser that provides the pixel-by-pixel mean lifetime retrieved by FAST-FLIM algorithm (see color bar from 0 to
7 ns), as well as a grey-scale inset image (see color bar from 0 to 255 counts) that provides the fluorescence intensity; (b)
same composite image FLIM and fluorescence intensity for the PZnAg:Eu glass; (c) intensity-weighted lifetime histograms for the
PZnAg and PZnAg:Eu glasses obtained from the FLIM images depicted in Figure 8a,b, respectively; and (d) normalized
fluorescence decays of both the PZnAg and PZnAg:Eu glasses and their ideal respective fittings with a four independent
exponential decay model. All data were obtained with a 435 nm pulse excitation of 6 ps at 4.75 MHz, and a collection over the
470–550 nm range.

As the fluorescence emission of the silver clusters corresponds to a broadband multi-
band emission that covers the whole visible range and depends on laser irradiation pa-
rameters, the fluorescence lifetime was also evaluated with a multiple exponential decay
model in the sub-ns and ns range. As detailed in the experimental section, curve fitting
with a multi-exponential decay model was performed on decays with better statistics,
corresponding to the binning of pixels of larger regions of interest. As shown in Figure 8d,
optimal time decay fitting was achieved with a four-exponential model with the adjusted
amplitudes and time constants being reported in the Table 1. Such non-usual fitting appeared to be necessary, and sufficient, to correctly fit the experimental decay with respect to standard acceptable statistical parameters. However, it is not attempted thereby to attribute each component to a precise population of emitters. This fitting is exclusively used to determine the average decay time, taking into account the statistical characteristics of single photon counting. The addition of components would not be meaningful, leading to covariance of the fitting parameters. Other models were not taken into consideration, since the estimation of an average value was sufficient in the context of this study, in order to characterize energy transfer efficiency. Still, the used model demonstrates that the complexity of lifetime decay of the system under investigation requires at least four typical decay times, but reality may be even more complex with additional, much shorter decay times.

Table 1. Fitting parameters with a four-exponential decay time model.

|     | τ<sub>i</sub> (ns) | A<sub>i</sub> (cts) | A<sub>i</sub> (%) |     | τ<sub>i</sub> (ns) | A<sub>i</sub> (cts) | A<sub>i</sub> (%) |
|-----|-------------------|-------------------|------------------|-----|-------------------|-------------------|------------------|
| Exp. #1 | 6.25             | 3527              | 3.3              | Exp. #1 | 5.75             | 2259              | 2.3              |
| Exp. #2 | 2.67             | 19008             | 17.7             | Exp. #2 | 2.19             | 16645             | 17.2             |
| Exp. #3 | 1.48             | 24017             | 22.4             | Exp. #3 | 0.92             | 25573             | 26.5             |
| Exp. #4 | 0.58             | 60861             | 56.7             | Exp. #4 | 0.42             | 52047             | 53.9             |

Based on the fitting results from the table, the intensity-weighted average emission lifetime τ<sub>int</sub> = (∑<sub>i=1..4</sub>A<sub>i</sub>τ<sub>i</sub>²)/(∑<sub>i=1..4</sub>A<sub>i</sub>τ<sub>i</sub>) of the PZnAg glass, and it decreases down to τ<sub>Ag,Eu</sub> = 1.94 ns in the Eu<sup>3+</sup>-containing glass, in agreement with the lifetimes denoted by the peak positions of the histograms of Figure 8c. This result corroborates the occurrence of energy transfer from Ag<sup>n+</sup> species levels to Eu<sup>3+</sup> ions. According to the expected lifetime of europium Eu<sup>3+</sup> in such glass, which is expected to be around a millisecond for the most intense emission around 612 nm, the collected decay measurement strictly corresponds to the silver cluster contribution.

To go further in the interpretation of energy transfers, based on the fitting results from Figure 8d and summarized in the table, the amplitude-weighted average emission lifetime τ<sub>ampl</sub> = (∑<sub>i=1..4</sub>A<sub>i</sub>τ<sub>i</sub>)/(∑<sub>i=1..4</sub>A<sub>i</sub>) was also estimated, leading to τ<sub>Ag</sub> = 1.34 ns and to τ<sub>Ag,Eu</sub> = 0.98 ns for the PZ:Ag and PZnAg:Eu glasses, respectively. The amplitude-weighted quenching rate Q<sub>Ag,Eu</sub> / τ<sub>Ag</sub> of the emitting silver clusters can be estimated as Q<sub>Ag,Eu</sub> / τ<sub>Ag</sub> = 1 - τ<sub>ampl</sub> / τ<sub>Ag</sub> < 27%. The comparison of the amplitude-weighted quenching rate Q<sub>Ag,Eu</sub> / τ<sub>Ag</sub> with the intensity quenching rate Q<sub>I</sub> / τ<sub>I</sub> < 41% helps in sorting the contributions of the emission quenching of the silver clusters. Indeed, the ratio Q<sub>Ag,Eu</sub> / τ<sub>Ag</sub> / Q<sub>I</sub> / τ<sub>I</sub> = 27%/41% < 66% indicates that 66% of the emission quenching of the silver clusters in presence of Eu<sup>3+</sup> ions is actually due to energy transfer. In addition, the estimation 1 - Q<sub>Ag,Eu</sub> / τ<sub>Ag</sub> / Q<sub>I</sub> / τ<sub>I</sub> < 33% indicates that 33% of the emission quenching of the silver clusters in the presence of Eu<sup>3+</sup> ions stands for a lower concentrations of silver emitters, affecting the fluorescence intensities but not the lifetimes. This can reasonably be interpreted by a slightly lower efficiency of silver cluster production during the femtosecond laser writing process. Indeed, in the laser inscription stage, we observed that Eu<sup>3+</sup> ions undergo multi-photon absorption and subsequent reddish fluorescence emission, which partially reduces the effective femtosecond laser intensity and thus completes the activation of the silver photochemistry and the associated creation and growth of silver clusters.

Regarding the europium emission intensity, the 612 nm Eu<sup>3+</sup> emission increases up to 5-fold and to 3.5-fold for excitations at 325 and 405 nm, respectively (Figure 9a,b), indicating an energy transfer from silver species to Eu<sup>3+</sup> ions [19,25,27]. The Eu<sup>3+</sup> emission
enhancement is clearly dependent on the excitation wavelength, as a larger efficiency is observed for an excitation at 325 nm. Such wavelength excitation dependence may be directly interpreted from Figure 5, with a more efficient excitation of silver clusters at 325 nm compared to 405 nm, leading thus to a more intense fluorescence emission and consequently to a larger amount of excited silver clusters compatible with resonant non-radiative energy transfers to Eu$^{3+}$ ions. Still, the existence of various populations of distinct silver clusters created during DLW has been reported [13], showing a partially selective excitation with radiations at 325 or 405 nm which may also play a selective role in the observed energy transfer. Indeed, these distinct types of silver clusters may show distinct energy transfer efficiencies to the Eu$^{3+}$ ions. The present spectroscopy cannot directly identify the nuclearities and associated stabilized redox charges of these silver species, nor their respective populations [13].

According to the singlet-triplet energy level model of Ag$_m^{n+}$ species proposed by Velazquez et al. [29] and to the results obtained from the phosphorescent excitation and emission spectra of the Eu$^{3+}$ and Ag$_m^{n+}$ species in the co-doped glass before and after laser–matter interaction, the energy transfer pathway was tentatively described in Figure 10. Under UV-visible light, Ag$^{+}$ ions and Ag$_m^{n+}$ species can be excited to the $S_1$ and $T_2$ energy levels, and then the $S_1 \rightarrow S_0$ and $T_2 \rightarrow S_0$ transitions may transfer the excitation energy to Eu$^{3+}$ by relaxations, thus populating the $^3H_3$ level and by non-radiatively relaxing from the $^5D_4$ and $^5I_6$ levels down to the $^5D_0$ energy level. The subsequent radiative transitions from the $^5D_0$ energy upper level leads to the visible Eu$^{3+}$ emissions observed in Figures 2 and 6. In addition, it is worth mentioning that the spin-forbidden transition of $T_2 \rightarrow S_0$ with relatively longer lifetime may mainly contribute to the above energy transfer processes. Still, at this level of description, the present spectroscopy cannot directly identify the mechanisms at play during the non-radiative resonant energy transfers; namely, one cannot directly discriminate between Dexter resonant energy transfers (DET) related to electron exchange operating at a very short scale (requirement of the wave function overlap) and Förster resonant energy transfers (FRET) related to dipole–dipole interactions spanning longer scales up to several nanometers typically (but highly sensitive to the solicited oscillation strength, which is known to be rather weak for the lanthanide ions) [30]. A balance between DET and FRET, both occurring simultaneously, may even exist. Such discrimination in the origin of the involved resonant energy transfer could further be addressed thanks to a set of glasses with various rare earth doping concentrations, which is beyond the scope of the present article.

Following the laser–matter interaction, a subsequent heat treatment performed at 400 °C ($T_g$ +20 °C) for 30 min in the glass revealed the crystallization of plasmonic silver nanoparticles. Such plasmonic structure precipitation will not be described in detail in the present paper, as they were investigated earlier by Marquestaut et al. [13]. These plasmonic structures led to a quenching of the energy transfer between Ag species and

Figure 9. Normalized amplitude of the micro-emission of the Eu$^{3+}$ fluorescence with respect to the pristine glass at 612.2nm, (a) for a 325 nm excitation and (b) for a 405 nm excitation, respectively showing up to 5-fold and 3.5-fold emission enhancements.
Eu$^{3+}$ ions, so that the enhancement of the Eu$^{3+}$ emission was mostly cancelled after thermal treatment, as shown in Figure 11 for an excitation at 325 nm. Indeed, the Eu$^{3+}$ emission enhancement ratio drops from 2.5- to 5-fold down to 1.2- to 1.8-fold (with an enhancement drop from 5-fold down to 1.2-fold for the highest laser-deposited dose from pattern C6). The precipitation of silver nanoparticles decreases the active population of silver clusters that can be excited and further transfer energy to Eu$^{3+}$ ions, thus reducing the energy transfer ability. Additionally, such silver nanoparticles can also contribute to quenching the fluorescence emission of the remaining silver clusters, further reducing the probability of energy transfer to Eu$^{3+}$ ions.

Figure 10. Energy level diagram showing schematically the possible energy transfer processes from Ag$_{nm}^{n+}$ to Eu$^{3+}$ (energy transfer labelled ET$_1$), and from Ag$^+$ to Eu$^{3+}$ (energy transfer labelled ET$_2$), upon excitation in the ultraviolet or visible range, leading to silver species emissions but also the indirect excitation of Eu$^{3+}$ and its emission in the visible.

Figure 11. Normalized amplitude of the micro-emission of the Eu$^{3+}$ fluorescence with respect to the pristine glass at 612.2 nm, for a 325 nm excitation before (dashed line, empty dots) and after thermal heat treatment (TT) at 400 °C ($T_g +20$ °C) for 30 min, showing both the decrease in the Eu$^{3+}$ fluorescence enhancement for high enough deposited laser doses (partial growth and subsequent destruction of populations of initially large silver clusters and correlative growth of metallic plasmonic silver NPs) also well as the minor but non-zero increase in the Eu$^{3+}$ fluorescence enhancement for lower deposited laser doses (partial growth from laser-induced defects or from populations of initially small silver clusters towards larger silver clusters that show a better resonant energy transfer toward Eu$^{3+}$ electronic levels.
4. Conclusions

Femtosecond laser inscription was achieved in a Eu$^{3+}$-doped silver-containing zinc phosphate glass, demonstrating that the insertion of rare earth ions does not inhibit the photo-activation of silver chemistry. By means of micro-spectroscopy of fluorescence emission, tri-chromatic coordinates in the CIE chromaticity diagram were estimated, showing that such coordinates can be continuously controlled from the red light aspect dominated by the Eu$^{3+}$ emission towards the white light aspect dominated by the silver cluster emission. This demonstrated the ability to perform a 3D-localized controlled modification of the local tri-coordinates thanks to the laser irradiation parameters. Compared to the pristine, Eu$^{3+}$ emission in the structured region showed an increase up to 5-fold and to 3.5-fold for excitations at 325 and 405 nm, respectively. Such an enhancement is co-localized with the fluorescent laser-inscribed silver clusters, which suggests a resonant non-radiative energy transfer from excited silver clusters to Eu$^{3+}$, thus allowing the fluorescence of the rare earth ion. FAST-FLIM imaging demonstrated the efficient resonant energy transfer from the silver clusters and to Eu$^{3+}$ ions. The precipitation of metallic silver plasmonic nanoparticles in the silver cluster location, obtained following heat treatment above glass transition temperature, removes the enhancement of the Eu$^{3+}$ emission. Femtosecond laser inscription in rare earth doped silver-containing glasses clearly demonstrates the effect of the silver cluster on the enhancement of europium ions and allows for writing 3D localized intense tunable emission patterns from red to white for a broad excitation spectrum in inorganic materials. This approach could be extended to other rare earth doped photosensitive glasses, including photo-thermo-refractive glasses [31], to promote 3D high-contrast luminescent patterns in various spectral ranges.

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