Abstract: Comparison of the shrinkage value of iron-based and non-ferrous metal alloys in the conditions of melts crystallization when using the quasi-equilibrium and non-equilibrium models was performed in the article. The ratios coefficients of cooling rates of alloys when the quasi-equilibrium and non-equilibrium crystallization models were obtained.

Key words: shrinkage, cooling, alloy, the quasi-equilibrium and non-equilibrium crystallization models.

Language: English

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**Introduction**

Crystallization of metal alloys in the various casting methods occurs in the certain temperature ranges: from the liquidus temperature ($T_{liq}$) to the solidus temperature ($T_{sol}$). The combination of the liquid and solid phases is formed in this range. The solid phase is in equilibrium with the liquid phase. This is due to low diffusion and convection of particles in alloy during cooling. The two-phase zone is described by sum of the several functions (bulk particles of the solid and liquid phases, voids when changing coordinates and time), which vary from 0 to 1. This is the main data for the quasi-equilibrium crystallization model of metal alloys.

The non-equilibrium crystallization model takes into account isolation of the various solid phases during solidification. The crystallization process occurs in the range from $T_{liq}$ to $T_{sol}$, and below $T_{sol}$.

Comparison of the quasi-equilibrium and non-equilibrium crystallization models will determine the ratio of changing cooling rates of melts in the mold and the predicted value of the changing shrinkage.

**Materials and methods**

Shrinkage and cooling rate of various metal alloys in the metal mold were determined. The calculation was performed when using the quasi-equilibrium and non-equilibrium crystallization models. The initial data for the experiment implementation were accepted: alloy steel – Fe (97.04%), C (0.4%), Si (0.27%), Mn (0.65%), Cr (0.95%), P (0.035%), S (0.035%), Cu (0.3%), Ni (0.3%), Al (0.02%), CLF up (70%), CLF down (30%), $T_0$ (1590 °C), $T_{liq}$ (1491.09 °C), $T_{sol}$ (1424.209 °C), $T_{eut}$ (1149.479 °C), $Q_{cr}$ (276 kJ/kg); carbon steel – Fe (98.19%), C (0.2%), Si (0.27%), Mn (0.5%), Cr (0.25%), P (0.035%), S (0.035%), Cu (0.25%), Ni (0.25%), Al (0.02%), CLF up (70%), CLF down (30%), $T_0$ (1610 °C), $T_{liq}$ (1512.896 °C), $T_{sol}$ (1472.422 °C), $T_{eut}$ (1142.583 °C), $Q_{cr}$ (271 kJ/kg); Qout (236.127 kJ/kg): chromium steel – Fe (85.74%), Cr (12.9%), Ni (0.12%), Si (0.54%), Mn (0.48%), C (0.07%), Cu (0.1%), Mo (0.02%), P (0.02%), S (0.01%), CLF up (70%), CLF down (30%), $T_0$ (1590 °C), $T_{liq}$ (1493.848 °C), $T_{sol}$ (1490.1 °C), $T_{eut}$ (1478.313 °C), $Q_{cr}$ (304 kJ/kg), Qout (304 kJ/kg); corrosion-resistant steel – Fe (69.75%), Ni (9%), Cr (18%), Si (0.5%), Mn (1.5%), C (0.12%), Cu (0.1%), Ti (1%), P (0.02%), S (0.01%), CLF up (70%), CLF down (30%), $T_0$ (1540 °C), $T_{liq}$ (1447.05 °C), $T_{sol}$ (1388.766 °C), $T_{eut}$ (1346.803 °C), $Q_{cr}$ (259 kJ/kg), Qout (259 kJ/kg); malleable cast iron – Fe (93.58%), C (3.6%), Si (2.5%), Mn (0.1%), P (0.02%), S (0.01%), Cu (0.15%), Mg (0.04%), CLF up (70%), CLF down (30%), $T_0$ (1250 °C), $T_{liq}$ (1157.94 °C), $T_{sol}$ (1150.51 °C), $T_{eut}$ (1150.421 °C), $Q_{cr}$ (160 kJ/kg), Qout (254.52 kJ/kg); grey cast iron – Fe (93.67%), C (3.35%), Si (2.05%), Mn (0.7%), P (0.15%), S (0.08%), CLF up (50%), CLF down (30%), $T_0$ (1270 °C), $T_{liq}$ (1178.297 °C), $T_{sol}$ (1150.075 °C), $T_{eut}$ (1150.064 °C), $Q_{cr}$ (160 kJ/kg), Qout (257.053 kJ/kg); white cast iron – Fe (63.25%), C (3%), Si (0.7%), Mn (0.6%), Cr (31%), P (0.1%), S (0.1%), Ni (1.25%), CLF up (70%), CLF down (30%), $T_0$ (1400 °C), $T_{liq}$ (1306.389 °C), $T_{sol}$ (1236.225 °C), $T_{eut}$ (1236.183 °C), $Q_{cr}$ (160 kJ/kg), Qout (242.99 kJ/kg); silumin – Al (87.81%), Si (11.5%), Mn (0.08%), Cu (0.1%), Fe (0.5%), Ti (0.01%), CLF up (70%), CLF down (30%), $T_0$ (690 °C), $T_{liq}$ (596.798 °C), $T_{sol}$ (576.09 °C), $T_{eut}$ (576.09 °C), $Q_{cr}$ (340 kJ/kg), Qout (505.611 kJ/kg); brass – Cu (60%), Zn (40%), CLF up (70%), CLF down (30%), $T_0$ (990 °C), $T_{liq}$ (898.128 °C), $T_{sol}$ (890.954 °C), $T_{eut}$ (419 °C), $Q_{cr}$ (136 kJ/kg), Qout (136 kJ/kg); magnesium alloy – Mg (93.4%), Al (3.1%), Mn (0.5%), CLF up (70%), CLF down (30%), $T_0$ (730 °C), $T_{liq}$ (632.002 °C), $T_{sol}$ (586.577 °C), $T_{eut}$ (390.66 °C), $Q_{cr}$ (293.6 kJ/kg), Qout (363.842 kJ/kg); nickel alloy – Ni (62.785%), Cr (9.5%), Al (4.4%), Co (13.5%), Ti (5.3%), W (1.4%), Mo (3%), B (0.15%), C (0.1%), CLF up (70%), CLF down (30%), $T_0$ (1380 °C), $T_{liq}$ (1282.978 °C), $T_{sol}$ (1267.638 °C), $T_{eut}$ (1223.505 °C), $Q_{cr}$ (297.4 kJ/kg), Qout (293.709 kJ/kg); nickel-cobalt alloy – Ni (80%), Co (20%), CLF up (70%), CLF down (30%), $T_0$ (1560 °C), $T_{liq}$ (1465.682 °C), $T_{sol}$ (1460.6 °C), $T_{eut}$ (1452 °C), $Q_{cr}$ (270 kJ/kg), Qout (270 kJ/kg); tin bronze – Cu (91%), Sn (9%), CLF up (70%), CLF down (30%), $T_0$ (1110 °C), $T_{liq}$ (1014.631 °C), $T_{sol}$ (862.914 °C), $T_{eut}$ (227 °C), $Q_{cr}$ (175.7 kJ/kg), Qout (175.7 kJ/kg); tinless bronze – Cu (95%), Al (5%), CLF up (70%), CLF down (30%), $T_0$ (1160 °C), $T_{liq}$ (1062.592 °C), $T_{sol}$ (1058.225 °C), $T_{eut}$ (1037 °C), $Q_{cr}$ (296.9 kJ/kg); zinc alloy – Zn (72.65%), Al (25%), Mg (0.1%), Cu (2.25%), Fe (0.7%), Pb (0.1%), Cb (0.1%), CLF up (30%), CLF down (30%), $T_0$ (580 °C), $T_{liq}$ (489.378 °C), $T_{sol}$ (377.686 °C), $T_{eut}$ (377.685 °C), $Q_{cr}$ (180 kJ/kg), Qout (123.269 kJ/kg).

**Results and discussion**

The experiment results were presented graphically. Two dependencies were built for comparison of the quasi-equilibrium and non-equilibrium crystallization models of metal alloys.

The dependencies of changing shrinkage of iron-based alloys from melt cooling rate are presented in the Fig. 1.
Impact Factor:

| Journal  | Impact Factor |
|----------|---------------|
| ISRA (India) | 4.971 |
| ISI (Dubai, UAE) | 0.829 |
| GIF (Australia) | 0.564 |
| JIF | 1.500 |
| SIS (USA) | 0.912 |
| PHHI (Russia) | 0.126 |
| ESJI (KZ) | 8.716 |
| ICV (Poland) | 6.630 |
| IBI (India) | 4.260 |
| ISI (Dubai, UAE) | 0.829 |
| GIF (Australia) | 0.564 |
| JIF | 1.500 |
| SIS (USA) | 0.912 |
| PHHI (Russia) | 0.126 |
| ESJI (KZ) | 8.716 |
| ICV (Poland) | 6.630 |
| IBI (India) | 4.260 |

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**Figure 1** – The dependencies of changing shrinkage of iron-based alloys from melt cooling rate: A – alloy steel, B – carbon steel, C – chromium steel, D – corrosion-resistant steel, E – malleable cast iron, F – grey cast iron, G – white cast iron. — the quasi-equilibrium crystallization model, — the non-equilibrium crystallization model.

Cooling rate of steels at the end of the crystallization process when using the quasi-equilibrium model is several times higher than cooling rate of steels at the end of the crystallization process when using the non-equilibrium model. Shrinkage of steels when the quasi-equilibrium and non-equilibrium crystallization models is almost the same. Maximum cooling rate is observed during crystallization of carbon steel.

Malleable and grey cast irons have different cooling rates. Maximum cooling rate (over 800 °C/s) is observed for cast irons at the end of the crystallization process when using the quasi-equilibrium model. Cooling rate of grey and malleable cast irons was determined in the range of 0-100 °C/s when the non-equilibrium crystallization model. Shrinkage of cast irons when the quasi-equilibrium crystallization model is 2.5-3 times less than when the non-equilibrium crystallization model. Calculated shrinkage for the two models is the same after crystallization of white cast iron.

Cooling rate of iron-based alloys has the negative values (the temperature decreases) in all cases, except for grey cast iron (the temperature of alloy increases at the certain phase section).

The dependencies of changing shrinkage of non-ferrous metal alloys from melt cooling rate are presented in the Fig. 2.

Cooling rates when using the considered crystallization models are different for non-ferrous metal alloys:
- maximum cooling rate of magnesium and zinc alloys is observed at the beginning of the crystallization process when using the non-equilibrium model;
- minimum cooling rate of nickel-cobalt alloy and tinless bronze is determined when the non-equilibrium crystallization model;
- increasing the temperature during cooling occurs only when the non-equilibrium crystallization model (brass, magnesium and zinc alloys).

The shrinkage value of non-ferrous metal alloys after crystallization is different for the two models. Shrinkage of alloys is less in the conditions of the non-equilibrium crystallization model.

The calculated values of the ratios coefficients of cooling rates of alloys when the quasi-equilibrium and non-equilibrium crystallization models are presented in the table 1.
Impact Factor:

| Journal  | Impact Factor |
|----------|---------------|
| ISRA (India) | 4.971 |
| ISI (Dubai, UAE) | 0.829 |
| GIF (Australia) | 0.564 |
| JIF | 1.500 |
| SIS (USA) | 0.912 |
| PRI (Russia) | 0.126 |
| ESJI (KZ) | 8.716 |
| IBI (India) | 4.260 |
| SJIF (Morocco) | 5.667 |
| OAJJ (USA) | 0.350 |

**Figure 2** – The dependencies of changing shrinkage of non-ferrous metal alloys from melt cooling rate: A – silumin, B – brass, C – magnesium alloy, D – nickel alloy, E – nickel-cobalt alloy, F – tin bronze, G – tinless bronze, H – zinc alloy. — the quasi-equilibrium crystallization model, — the non-equilibrium crystallization model.

**Table 1.** The ratios coefficients of cooling rates of alloys when the quasi-equilibrium and non-equilibrium crystallization models.

| Alloy                | Coefficient |
|----------------------|-------------|
| Alloy steel          | -0.7166666666666666666337 |
| Carbon steel         | -4.4489795918367346938606448979592 |
| Chromium steel       | 0.6325088392226148410064770318021 |
| Corrosion-resistant steel | 4.9999999999999999949675 |
| Malleable cast iron  | -105.666666666666666665639 |
| Grey cast iron       | 24999.9999999 |
| White cast iron      | -1.239436619718309859215661971831 |
| Silumin              | 2.333333333333333333333333333333333 |
| Brass                | 0.966610169491559237289488135593219 |
| Magnesium alloy      | 3.1052631578947368421145789473684 |
| Nickel alloy         | 16.333333333333333333333333333333333 |
| Nickel-cobalt alloy  | 4.62499999999999999999998335 |
| Tin bronze           | -1.9354838709677419354412903225806 |
| Tinless bronze       | 5.9241542915774784790973180985915 |
| Zinc alloy           | 0.98591549295774647890971830985915 |

The significant changing ranges of cooling rates are dominated in grey and malleable cast irons in comparing the two considered crystallization models. The negative value of the coefficient indicates the positive and negative values of cooling rate of alloys for the two considered crystallization models.

**Conclusion**

1. Cooling rate and the shrinkage value of malleable and grey cast irons when the quasi-equilibrium and non-equilibrium crystallization models are different and vary several times. Almost identical cooling rates are observed during crystallization of steels.
2. It is determined that the cooling temperature increases over the certain time range during non-equilibrium crystallization of grey cast iron, brass, magnesium and zinc alloys.

3. The ratios of cooling rates of corrosion-resistant steel and nickel-cobalt alloy, brass and zinc alloy during quasi-equilibrium and non-equilibrium crystallization are almost the same.

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