Abstract

Nanoscale electrostatic microtubule disassembly forces between positively charged molecules in kinetochores and negative charges on plus ends of microtubules have been implicated in poleward chromosome motions and may also contribute to antipoleward chromosome movements. We propose that chromosome congression can be understood in terms of antipoleward nanoscale electrostatic microtubule assembly forces between negatively charged microtubule plus ends and like-charged chromosome arms, acting in conjunction with poleward microtubule disassembly forces. Several other aspects of post-attachment prometaphase chromosome motions, as well as metaphase oscillations, are consistently explained within this framework.

Introduction

Poleward and antipoleward chromosome movements occur intermittently during prometaphase and metaphase. Poleward motion dominates during anaphase-A, while antipoleward motions dominate during the congressional movement of chromosomes to the cell equator. The apparent complexity of these motions has challenged scientific explanation for over a hundred years.

Experiments have shown that during prometaphase each pair of sister chromatids attaches by a kinetochore to the outside wall of a single microtubule, resulting in a rapid microtubule sliding movement toward a pole [1]. This motion is generally thought to be driven by molecular motors; specifically, the speed (20–50 μm per minute) of kinetochores along microtubule walls is consistent with known molecular motor behavior [1]. Current thought on chromosome motility, however, does not appear to favor molecular motors for post-attachment force generation.

As discussed elsewhere [2–5], force generation by nanoscale electrostatic microtubule disassembly forces between positive charges at kinetochores and negative charges on microtubule plus ends may be responsible for chromosome poleward motility during mitosis. We propose here that antipoleward nanoscale electrostatic microtubule assembly forces acting at chromosome arms combined with poleward forces are responsible for chromosome congression, and that this combination is consistent with other post-attachment prometaphase motions as well as metaphase chromosome oscillations.

The approach of kinetochores to the poles result in their movement to within critical distances of the ends of other (astral) microtubules emanating from the closer pole. Importantly, electrostatic forces increase significantly between charged surfaces separated...
by 3 nm or less (see below). The resulting proximity—in conjunction with (1) an electro-
static attraction between positively charged kinetochores and negatively charged ends
of astral microtubules, (2) an electrostatic repulsion between negatively charged
chromosome arms in the chromatid pair and neighboring negatively charged astral
microtubule ends, and (3) constant thermal agitation—is likely integral to the orientation
and end-on attachment of kinetochores to free microtubule plus ends [2]. Following a
monovalent (or mono-oriented) attachment to one pole, chromosomes subsequently move
at considerably slower speeds (a few μm per minute) throughout prometaphase [6]. In
particular, a period of slow movements toward and away from a pole ensues until close
proximity of the free microtubule end with the other (sister) kinetochore in the chromatid
pair results in a bivalent (bioriented) attachment. Attachments of additional microtubules
from both poles follow. After a sister kinetochore becomes attached to microtubules from
the opposite pole, the chromosomes perform a slow (1–2 μm per minute) congressional
motion to the spindle equator, resulting in the well-known metaphase alignment of
chromatid pairs [6].

**Antipoleward nanoscale electrostatic assembly force**

The permittivity \((k \varepsilon_o)\) of the first few water layers outside a charged surface is an order
of magnitude smaller than that of the bulk phase [7], and the effective permittivity of
water as a function of distance from a charged surface increases monotonically from
4–6 \(\varepsilon_o\) at the interface to 78 \(\varepsilon_o\) at a distance of 25 nm from the interface. The values of
the dielectric constants \(k(x)\) at distances \(x\) of 1, 2, 3, and 4 nm from a charged surface
are 9, 21, 40, and 60, respectively [8]. Additionally, layered water adhering to charged
molecules greatly reduces counterion (Debye) screening for small distances from their
surfaces. Such water layering to charged proteins (e.g., microtubules) has long been
theorized [9,10], and confirmed experimentally [11].

The interpolated values of \(k(x)\) for separations between charged surfaces of up to
3 nm are 5, 9, 9 and 5 for \(x = 0, 1, 2\) and 3 respectively, where the charged surfaces
are at \(x = 0\) and \(x = 3\) nm (the experimental value of \(k(x)\) at both \(x = 0\) and \(x = 3\) is 5,
and symmetry and the experimental numbers dictate the values of 9 in between). The
distance range of 1–3 nm between charged molecular surfaces is appropriate because
1 nm may be taken as the thickness of layered water adsorbed to each charged surface
[10,12], and for charged molecular surface separations up to 3 nm, counterion screening
would be virtually eliminated. Thus electrostatic force is increased over the distances
allowed by reduced Debye screening, and is further increased (by an order of magnitude)
due to an order of magnitude reduction in the dielectric constant between the charged
surfaces. For brevity, separations of up to 3 nm (and – due to the reduced dielectric
constant between charged molecular surfaces – 1 to 2 nm beyond) between charged
surfaces will hereafter be designated as critical distances/gaps.

Due to the strong negative charge carried by chromosome arms, they are repelled from
negatively charged free ends of astral microtubules in the polar region. Microtubule
polymerization occurs in relatively large gaps that result from smaller (near critical)
gap-dependant electrostatic repulsion between negatively charged microtubule plus
ends and negatively charged chromosome arms. This process continues with other
constantly changing subsets of smaller and larger gaps, causing chromosomes to be
continuously repelled from poles. This mechanism may account for the antipoleward *astral exclusion force*, or *polar wind*, the precise nature of which has been sought since it was first observed [13]. The interaction between astral microtubules and chromosome arms is depicted in Figure 1.

As a chromatid pair moves farther from a pole, electrostatic repulsive forces between the negatively charged free ends of astral microtubules and chromosomes decreases as the microtubules fan radially outward. At a surface defined by the microtubule ends, the charge density and therefore the force, will decrease according to an “inverse square law”. Specifically, the repulsive force on a chromosome arm depends on the total number $N$ of negatively charged microtubule free ends from which it is repelled; thus $F \sim N q$, where $q$ is the charge at the end of a microtubule. For $N$ microtubules fanning radially outward from a pole, the total charge $N q$ is distributed over an area that increases as the distance $r$ from the pole squared ($r^2$), and the effective charge per unit area at a surface defined by the microtubule ends decreases as the inverse of the distance squared ($1/r^2$). This results in a nanoscale repulsive electrostatic antipoleward force on chromosome arms that decreases with an inverse square ($1/r^2$) dependence on the polar distance.

The falloff is even more pronounced than an inverse square dependence predicts due to the decreased number of microtubule free ends more distant from the poles, thus
further reducing the antipoleward force (Figure 2). We refer to this effect as the robust inverse square antipoleward force.

**Prometaphase and metaphase chromosome motions**

Microtubule polymerization and depolymerization, in combination with poleward and antipoleward forces, are sufficient to account for the observed motion of monovalently attached chromosomes. Due to fluctuations in both the number of disassembling kinetochore microtubules (interacting with kinetochores and centrosomes), and in the number of assembling astral microtubules (responsible for the antipoleward force acting at chromosome arms), these opposing forces result in a “tug of war” consistent with experimentally observed movements toward and away from a pole for a monovalently attached chromatid pair [6].

After a bivalent attachment is established, the attractive force to the distal pole opposes the attractive force to the proximal pole. The robust inverse square astral exclusion force results in greater repulsion from the proximal pole, and combined with a growing number
of kinetochore attachments to microtubules from the distal pole (tending to equalize poleward disassembly forces), generates a relatively sustained congressional motion away from the proximal pole, as observed experimentally [6]. We emphasize that—within the context of our model—the dominance of the robust inverse square antipoleward force from the proximal pole is primarily responsible for chromosome congression. While some studies suggest that chromokinesins are involved in generating antipoleward force, others indicate that they are not essential for chromosome congression [14]. Note also that microtubule assembly at kinetochores and poles can occur; however, because the necessary inverse square dependence of the antipoleward microtubule assembly force cannot be derived from microtubule assembly at kinetochores or spindle poles, it is likely that assembly at either location is in passive stochastic response to assembly at chromosome arms, or to tension caused by poleward forces on sister kinetochores.

As a chromatid pair congresses to the midcell region, the number of attachments to both poles will tend to be the same as will the number of microtubules interacting with chromosome arms, and thus equilibrium of poleward directed forces and antipoleward astral exclusion forces will be approached. Without specifying their exact nature, such balanced pairs of attractive and repulsive forces have previously been postulated for the metaphase alignment of chromatid pairs [15].

An explanation of experimentally observed mid-cell metaphase oscillations just prior to anaphase-A provides an example of the predictability and minimal assumptions nature of the model. In agreement with experimental observations [16], our model predicts that the poleward force on a chromosome from kinetochore microtubule disassembly (at kinetochores and poles) depends on the total number of kinetochore microtubules. At the metaphase “plate”, the bivalent attachment of chromatid pairs ensures that the poleward-directed electrostatic disassembly force on one chromatid at a given moment could be greater than that of the sister chromatid’s kinetochore attached to the opposite pole. An imbalance of these poleward forces results from statistical fluctuations in the number of force generating kinetochore microtubules. This situation, coupled with similar fluctuations in the number of astral microtubules responsible for the antipoleward astral exclusion force on a chromatid pair, can result in a momentary motion toward a pole in the direction of the instantaneous net force. However, due to the robust inverse square dependence of the repulsive astral exclusion force and the approximate equality of poleward-directed microtubule disassembly forces for chromatid pairs in the midcell region, the greater force of repulsion from the proximal pole will eventually reverse the direction of motion resulting in midcell metaphase oscillations, as observed experimentally [6].

Midcell metaphase oscillations are indirect evidence for a continuing increase in the disassembly to assembly probability ratio resulting in parity for microtubule assembly and disassembly probabilities. As discussed elsewhere [17], this continuing increase in the microtubule disassembly/assembly ratio may be due to a continuously decreasing intracellular pH (pHi). At late metaphase, before anaphase-A, experiments reveal that poleward motions of sister kinetochores stretch the intervening centromeric chromatin producing high kinetochore tensions, most likely caused by a continuing disassembly to assembly probability ratio increase. At these high tensions, microtubule plus ends often switch from a depolymerization to a polymerization state of dynamic instability. This may
be explained by kinetochore microtubule free ends taking up the slack by polymerization to sustain attachment and resist further centromeric chromatin stretching, collectively known as the “slip-clutch mechanism” [18,19], as explained below.

Microtubule assembly at a kinetochore or a pole is regarded here as operating in passive response to (1) the robust inverse square electrostatic antipoleward force acting between the plus ends of microtubules and chromosome arms and/or (2) an electrostatic microtubule disassembly force at a sister kinetochore or at poles. At the highest tensions, electrostatic forces acting over critical distances between protofilament free ends and kinetochores are effective in maintaining coupling while larger protofilament gaps in the same or other microtubules are passively filled in. Additionally, the robust inverse square microtubule assembly force acting at a sister chromatid’s arms provides a feedback mechanism to resist detachment. This explanation of the slip-clutch mechanism follows as a direct consequence of the proposed model with no additional assumptions. As discussed elsewhere [17], anaphase-A results from the eventual complete domination of microtubule disassembly over assembly, resulting in a poleward disassembly force that dwarfs the antipoleward microtubule assembly force.

**Conclusions**

Both the range and strength of electrostatic forces within cells is greater than counterion screening would dictate. Chromosome congression likely results from a combination of poleward forces with a robust inverse square antipoleward electrostatic microtubule assembly force acting at chromosome arms. The dominance of the inverse square dependence of the antipoleward microtubule assembly force over the poleward microtubule disassembly force is primarily responsible for chromosome congression as well as metaphase chromosome oscillations. Chromosome end-on attachment orientation and the “slip-clutch” mechanism are consistent with this combination of opposing forces.

**Competing interests**
The authors declare that they have no competing interests.

**Authors’ contributions**
DHS made intellectual contributions and drafted the manuscript. LJG conceived the study. All authors read and approved the final manuscript.

**Acknowledgements**
We thank Rutgers University for providing the infrastructure to complete this manuscript.

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Received: 24 October 2013 Accepted: 12 February 2014
Published: 24 February 2014

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