On the Impact of Solvation on a Au/TiO₂ Nanocatalyst in Contact with Water

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Water, the ubiquitous solvent, is also prominent in forming liquid-solid interfaces with catalytically active surfaces, in particular with promoted oxides. We study the complex interface of a gold nanocatalyst, pinned by an F–center on titania support, and water. The ab initio simulations uncover the microscopic details of solvent-induced charge rearrangements at the metal particle. Water is found to stabilize charge states differently from the gas phase as a result of structure-specific charge transfer from/to the solvent, thus altering surface reactivity. The metal cluster is shown to feature both “cationic” and “anionic” solvation, depending on fluctuation and polarization effects in the liquid, which creates novel active sites. These observations open up an avenue toward “solvent engineering” in liquid-phase heterogeneous catalysis.

Highly dispersed gold nanoparticles supported on oxides have been shown to catalyze a number of important reactions, including low–temperature CO oxidation and the water gas shift reaction \[ \text{CO} + \text{H}_2 \rightarrow \text{CH}_4 + \text{H}_2 \text{O} \]. Reducible oxides, in particular titania (TiO₂), are ideal catalytic supports. The size of the gold particles substantially affects the catalytic activity, suggesting the key importance of metal/support interactions on a nanometer scale. Reactions, and in particular CO oxidation, are believed to occur at specific active Au sites at the Au/TiO₂ interface. Although much is known regarding Au/TiO₂ catalytic activity in the presence of a gas phase, the complexity increases steeply when solvent is included.

Liquid–solid interfaces as such are relevant to many industrial applications of great significance, such as (photo-)catalysis, solar cells, gas sensors, or biocompatible devices. In heterogeneous catalysis, it has been shown that the presence of water increases the observed rate of CO oxidation. The degree of rate enhancement depends on the type of support used. In particular for the case of Au/TiO₂ catalysts it has been shown that their activity at about 3000 ppm H₂O is so high that full conversion of CO is reached. Thus, the Au/TiO₂ surface displays a pronounced catalytic activity toward the water-gas-shift (WGS) reaction. This fundamental reaction represents a key reaction to produce extra H₂ fuel from steam reforming, which is reversible and exothermic, according to the following reaction: \[ \text{CO} + \text{H}_2 \text{O} \leftrightarrow \text{CO}_2 + \text{H}_2 \]. The so-called carboxyl and redox mechanisms have been proposed for the WGS reaction on metal/oxide surfaces; in the former mechanism the CO species reacts with terminal hydroxyl groups, whereas in the latter CO reacts with an O atom from OH dissociation or from the oxide support. In both mechanism proposed the starting point is a H₂O molecule that is initially adsorbed on the metallic cluster with its oxygen atom being attached to a metal atom.

Moreover, even large (as opposed to nanoscale) gold particles, which are usually catalytically inert, show considerable oxidation activity at aqueous conditions. Because of its high dielectric constant, water may actively participate in chemical reactions for instance by stabilizing ionic species, thus speeding up reactions at liquid-solid interfaces, which opens up novel avenues to improve the performance of traditional heterogeneous catalysis at the gas-solid interface. Recently, it has been shown that the selective oxidation of alcohols in aqueous phase over (TiO₂, C)–supported Au catalysts is facilitated by high pH conditions. This water-based approach to heterogeneous catalysis offers a sustainable, environmentally benign, and cheap alternative to traditional processes that rely on both toxic and expensive inorganic oxidants and organic solvents. Despite these promising experimental findings, much remains unknown at the molecular level about the impact of water as a solvent on the reactivity of these modern catalyst systems.

Several ab initio molecular dynamics (AIMD) studies have been recently reported focussing on the fundamentals of the water-titania interface. For a water film on TiO₂(110) it has been shown that at least two distinct layers form: molecules in the first layer are sluggish and bind strongly to fivefold coordinated Ti sites, whereas those in the second layer interact only weakly with the substrate and diffuse rapidly, thus yielding a highly anisotropic interface. Moreover, water was not seen to dissociate at the coverages examined. Upon studying the thermodynamics of de/protonation of the rutile-water interface using free energy perturbation methods, a value of 0.6 eV was found for the dissociation free energy of bulk water on defect-free rutile. These studies thus show that the ideal TiO₂ surface is rather inert with respect to solvation by water. However, little is known about the interaction between water and defective or metal-supporting TiO₂ interfaces, being relevant to catalysis and industrial applications.

Here, we present large-scale AIMD simulations aimed to investigate solvent effects at a gold nanocluster pinned by an F–center on TiO₂(110) being in contact with liquid water. The aqueous solution is found to induce pronounced charge transfer and localization at the
nanocatalyst–liquid interface and stabilizes structures different from the gas phase. The TiO$_2$(110) surface has been modeled by four O–Ti$_2$O$_2$–O tri-layer (4×2) supercell slabs separated by more than 15 Å. The most common point defects on the TiO$_2$(110) rutile surface are oxygen vacancies in the twofold coordinated O rows. Therefore, a Au$_{11}$ nanocluster was grown on TiO$_2$(110) where an F–center created by a surface O vacancy acted as anchoring site for initial Au nucleation; note that this blocks the O defect to interact with water and thus prevents splitting of water molecules at this F–center. The lowest energy structure of Au$_{11}$ adsorbed on a reduced rutile surface and employed in the present study is shown in Fig. 1(c)). In order to create the Au$_{11}$/TiO$_2$–water interface, the space between the slabs has been fully filled with 53 H$_2$O molecules (see Fig. 1(a)). It has been shown that Au$_{17}$ is the smallest Au cluster on rutile TiO$_2$(110) with a measurable reaction rate for CO combustion [19]. The Au$_{11}$ model, although being a simplification of the nanometersized clusters on TiO$_2$(110), appropriately mimics the active sites located at the nanogold/oxide interface where the oxidation process takes place [6, 20].

![Image](image_url)

**FIG. 1:** Ball and stick model of the Au$_{11}$ nanocluster pinned by an F–center on the TiO$_2$(110) oxide surface in contact with liquid water (a) and with a gas phase (c). Red, big blue, small blue and brown spheres are O, Ti, H and Ti$_{3+}$ sites, respectively, whereas the surface O vacancy is shown in green. Violet, black and yellow spheres correspond to top, middle and bottom Au sites of the Au$_{11}$ nanocluster, respectively. Time evolution of the Löwdin charges of the top (violet lines) and middle (black lines) Au atoms of the supported gold nanocluster in liquid water (b) and in the gas phase (d). Red and orange triangles correspond to reference Löwdin charges computed for a single Au$^+$ (aq) cation (10.924 [e]) and Au$^{2+}$(aq) atom (11.210 [e]) in liquid water, respectively.

The binding of the Au$_{11}$ cluster on the reduced TiO$_2$(110) support entails a strong charge rearrangement at the metal/oxide contact (see Supporting Figure 1), the adsorption energy being −2.19 eV. In the case of an isolated O vacancy on the stoichiometric TiO$_2$(110) surface, the charge neutrality is maintained by the presence of two Ti$_{3+}$ ions thus creating an F–center. Spin density and bonding charge analyses reveal that the Au$_{11}$ cluster, once adsorbed, leaves a reduced substrate with three Ti$_{3+}$ ions, and ~0.4 [e] are transferred from the metal cluster to the oxide. This results into a slightly positively charged Au$_{11}^{2+}$ cluster supported by a reduced TiO$_2$(110) oxide surface.

In order to reveal the solvent-induced charge rearrangement at the metal-liquid contact, we have performed PBE + U AIMD simulations of the Au$_{11}$/TiO$_2$(110) nanocatalyst in aqueous solution. Additionally, corresponding gas phase simulations have been carried out to provide the solvent-free reference situation. In both cases the finite temperature dynamics preserves three reduced Ti$_{3+}$ sites (see Supporting Figure 2). Snapshots of the AIMD simulations have been collected every ~0.2 ps thus generating a set of representative configurations for electronic structure analyses. In the following, we will refer to Au atoms of the supported Au$_{11}$ nanocluster as top, middle and bottom sites, which are depicted as violet, black and yellow spheres in Fig. 1, respectively. A detailed investigation of the interaction between H$_2$O molecules and the bare oxide surface far from the supported metal cluster is out of the focus of this study, but we note in passing that our AIMD simulations are in agreement with those of [18] in the regions. In particular, water at the liquid–oxide contact is slow, strongly bonded to fivelfold coordinated Ti sites, and is not seen to dissociate.

The charge dynamics of the Au sites was extracted by computing, as a function of time, the Löwdin charges, see Fig. 1, where violet and black lines correspond to the charge evolution of top and middle Au atoms, respectively. As demonstrated by Fig. 1(b), two distinct charge patterns, corresponding to top and middle Au sites, can be clearly distinguished in aqueous solution; note that Au atoms in direct contact with TiO$_2$ (yellow spheres in Fig. 1(a)) cannot be solvated by the liquid phase and thus do not exhibit a clear trend. The average charges on top and middle Au atoms are 11.028 ± 0.006 and 11.220 ± 0.006 [e], respectively (see Supporting Table 1 for statistical analysis). It is noted in passing that a very similar charge separation has been found for a gold cluster of different size and shape using an Au$_{13}$/TiO$_2$(110) nanocatalyst in contact with water. Interestingly, at around 6 ps a considerable amount of charge is transferred to a specific top Au site due to solvent fluctuations, which reaches a value that is typical of middle Au atoms, see Fig. 1(b). In stark contrast, no such charge separation and fluctuation effects can be identified in the...
FIG. 2: Dynamics of the water = nanocluster charge transfer (CT). Violet and black lines correspond to top and middle Au atoms, respectively.

gas phase reference dynamics in Fig. 4(d). We conclude that the liquid phase promotes and stabilizes a net charge separation in the supported Au cluster, where top and middle atoms can be clearly distinguished on the basis of their electronic structure. As a result, water steers the Au sites towards either one or the other preferred charge value, depending on their specific location within the nanocluster and going hand in hand with different solvation patterns, vide infra.

To further characterize this puzzling process we have quantified the amount of charge transfer (CT) from Au atoms to the aqueous solution and back using Bader analysis [23, 24]. For this purpose we have computed the difference between the Bader charges of the Au atoms in the fully solvated Au11/TiO2(110)–water system and those of the corresponding Au11/TiO2(110) gas phase system, where the latter is obtained upon removing the solvent while keeping all atomic positions fixed. As depicted in Fig. 2 we find that top Au sites transfer charge to the solvent, with an average CT of about 0.13 ± 0.05 |e|, while middle Au atoms attract about 0.06 ± 0.03 |e| per Au atom from water.

In view of these pronounced CT effects, we probe solvent-induced morphology changes of the metal cluster with respect to the gas phase. A set of trajectory configurations of the solvated nanocatalyst has been selected where water has been removed before quenching and optimizing the remaining Au11/TiO2(110) system. In order to generate the proper gas phase reference, Au11/TiO2(110) in the absence of water has been run at the same temperature of 450 K before applying the same quenching protocol; note that this is the relevant experimental temperature used for selective liquid–phase alcohol oxidation in aqueous solution using gold/titania catalysts. In case of the quenched solvated interface, the same local minima and no significant change in the Löwdin charges were observed as in the solvated state. However, the gas phase reference system yielded several local minima with significant changes of both the real-space structure and the Au charges (see Supporting Figures 3 and 4). These findings show that the liquid phase stabilizes structures and charge states within nanogold that are distinctly different from those observed in the gas phase, which eventually induces novel morphologies and active sites, respectively, due to solvation.

Let us now investigate the solvent-induced electronic charge redistribution at the nanocatalyst. In the following, we refer the electronic charge density of the solvated Au11/TiO2(110)–water system to that of the isolated one, Au11/TiO2(110), and the separated solvation water. We thus compute the difference, \( \Delta \rho(\vec{r}) \), between the charge densities of the combined system and the separated components while freezing all atomic positions fixed. A representative example of water-induced charge flow is depicted in Fig. 4 where the positive (negative) component of the charge difference \( \Delta \rho_+(\vec{r}) \) is shown by red (blue) isosurfaces. This reveals that charge depletion (blue) occurs mainly on top Au atoms, whereas additional electron charge (red) prefers to accumulate on middle Au sites. Furthermore, charge depletion and accumulation visible at the oxide-water contacts can be traced back to the interaction between water and the TiO2(110) oxide support. Here charge depletion occurs mainly on top of surface O atoms to which H2O molecules point their H atoms, whereas charge accumulates close to five-fold coordinated Ti atoms, being in turn coordinated by water O atoms. This is quantified by considering the charge redistribution perpendicular to the support, \( \Delta \rho(z) \) (see Fig. 5). Here \( \Delta \rho(z) \) is the sum of the positive and negative charge density components and integrated in planes perpendicular to the surface. This quantitative analysis reveals that, on the one hand, there is a net charge transfer of ~ 0.22 |e| from top Au atoms to H2O molecules (obtained by integrating \( \Delta \rho(z) \) within the shaded orange area in Fig. 5), leading to slightly positively charged Au\(^{4+}\) atoms at the corresponding sites.
On the other hand, there is a reverse charge flow of \( \sim 0.37 \) \( |e| \) from water to middle Au atoms (see yellow area in Fig. 4(a), thus creating partially negatively charged Au\(^{2-}\) atoms upon solvation. Similar results were obtained for all the representative structures sampled along the trajectory. This can be compared to the average negative and positive CT obtained from the Bader analysis. In total, this amounts to a structure-specific charge exchange between metal and water of \(-0.34\) and \(+0.46 \) \( |e| \), in qualitative agreement with the charge difference analysis. As a result, top and middle Au sites experience opposite charge flow upon interaction with the solvent, as clearly shown in Fig. 3 which connects to a peculiar solvation pattern.

We thus conclude by discussing the solvation pattern around the Au\(_{11}\)/TiO\(_2\)(110) nanocatalyst, see Fig. 4(a), which is found to feature both so-called “cationic” and “anionic” solvation depending on fluctuation and polarization effects. This is similar to what we have observed previously for a single Au\(^{+}\)(aq) cation and neutral atom, Au\(^0\)(aq), in aqueous bulk solution [23]. In particular, the Au\(^+\) aqua ion forms a quasi-linear molecular structure, H\(_2\)O-Au\(^+\)-OH\(_2\), in which two water molecules are firmly bound through their oxygens to the Au\(^+\) site, as expected for a cation, yielding an Au\(^+\)-O distance of \( \sim 2.04 \) Å. Upon adding an electron to Au\(^+\) to yield Au\(^0\), we found that its solvation pattern changes distinctly. The latter features two distinct regions, supporting a Janus-type behavior. In one region a typical anionic solvation pattern prevails where two water molecules are pointing with their H atoms toward the metal. In other regions water binds via its O site to the Au\(^0\)(aq), thus giving rise to a typical cationic solvation pattern.

Around the nanocatalyst, two distinct solvation patterns corresponding to different Au charge states can be identified. The solvation around middle Au atoms consists of H\(_2\)O molecules pointing with their H atoms toward the Au atoms like in an anionic solvation shell. In addition, several water exchange processes are observed as for Au\(^0\)(aq) in the bulk [23]. At variance with those sites, the solvation around top Au atoms features a typical cationic solvation pattern, where a single H\(_2\)O molecule point to a top Au atom via its O site. A projected density of states analysis reveals that the interaction between gold atoms and solvating water molecules results from the overlap between the Au(d) and O(p) states of the respective gold and oxygen sites. Interestingly, no H\(_2\)O exchange processes are observed in this case again in line with the Au\(^+\)(aq) cation case [23]. As depicted in Fig. 4(b) the Au\(^+\)(aq) cation and neutral atom, Au\(^0\)(aq), cation case [23]. As depicted in Fig. 4(b) we plot the distances between the top Au atoms with typical “cationic” solvation pattern and the O atom of its solvating H\(_2\)O molecule. This demonstrates that two Au atoms are always “bonded” to the the same H\(_2\)O molecule along the full trajectory, the time-averaged distances between Au and O sites being 2.25 and 2.35 Å. The situation is very different at the third top Au site. This Au atom is initially cationically solvated yielding a Au–O distance around 2.3 Å. At \( \sim 6 \) ps the H\(_2\)O molecule rearranges and points to the same gold atom with one of its H atoms, a fluctuation which induces the change of charge state of this Au site discussed earlier. This reveals the intimate connection between the creation of excess charge at specific nanocluster sites and the preferential orientation of the interfacial water molecules. As discussed in the introduction for the carboxyl and redox mechanisms proposed for the WGS reaction on metal/oxide surfaces, the first step involves H\(_2\)O molecules that are initially adsorbed on the metal cluster such that their O atoms are coordinated to an Au site. Therefore our simulations suggest that top site Au atoms, which feature a typical “cationic” solvation pattern at the water-gold interface, are the most promising candidates for being the active site for CO oxidation via the WGS reaction, whereas “anionically” coordinated Au sites are expected to be chemically inert. The very same argument will hold for other liquid-phase catalytic reactions – thus providing a novel mechanism to create active sites at catalyst–water interfaces in much more general terms.

In conclusion, finite temperature PBE + U simulations have been employed to investigate solvent-metal interactions on the gold/titania nanocatalyst in liquid water. Comparing our liquid phase to gas phase and bulk solvation reference data demonstrates that interfacial water alters both the structure and electronic properties of the
supported metal cluster in a significant way, including the creation of active sites. The fundamental phenomena observed will have a profound impact on understanding the role of solvent in heterogeneously catalyzed liquid-phase reactions, where de- and re-solvation processes play a key role.

Methods

All calculations have been performed using spin-polarized PBE + U [29], and ultrasoft pseudopotentials [29] as implemented in CPMD [23, 24], and Quantum Espresso [23]. In line with our previous work [23, 24], the value of U = 4.2 eV was adopted. We have carefully checked the charge distribution dependence on U by re-computing the Löwdin charges of the top and middle Au atoms of the supported gold nanocluster in liquid water for selected snapshots along the trajectory shown in Fig. 1(b) using four different U values and found no significant change (see Supporting Material for data).

The AIMD simulations [29] used Car–Parrinello propagation, the canonical ensemble was established at 450 K with a Nosé-Hoover chain thermostat, and about ∼10 ps trajectories have been generated for analysis (see Supporting Material for details).

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Supporting Information
Detailed descriptions of methods used for the calculations, model system and and much additional analyses. This material is available free of charge via the Internet at [http://pubs.acs.org](http://pubs.acs.org)

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