Search for the decay modes $D^0 \to e^+ e^-$, $D^0 \to \mu^+ \mu^-$, and $D^0 \to e^\pm \mu^\mp$

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D0 → ℓ+ℓ− and D0 → D0 mixing in new physics models has also been emphasized [2].

We search for D0 → ℓ+ℓ− decays using approximately 468 fb−1 of data produced by the PEP-II asymmetric-energy e+e− collider [3] and recorded by the Babar detector. The center-of-mass energy of the machine was at, or 40 MeV below, the T(4S) resonance for this dataset. The Babar detector is described in detail elsewhere [4]. We give a brief summary of the main features below.

The trajectories and decay vertices of long-lived hadrons are reconstructed with a 5-layer, double-sided silicon strip detector (SVT) and a 40-layer drift chamber (DCH), which are inside a 1.5 T solenoidal magnetic field. Specific ionization (dE/dx) measurements are made by both the SVT and the DCH. The velocities of charged particles are inferred from the measured Cherenkov angle of radiation emitted within fused silica bars, located outside the tracking volume and detected by an array of phototubes (DIRC). The dE/dx and Cherenkov angle measurements are used in particle identification. Photon and electron energy, and photon position, are measured by CsI(Tl) crystal calorimeter (EMC). The steel of the flux return for the solenoidal magnet is instrumented with layers of either resistive plate chambers or limited streamer tubes [5], which are used to identify muons (IFR).

I. INTRODUCTION

In the Standard Model (SM), the flavor-changing neutral current (FCNC) decays D0 → ℓ+ℓ− are strongly suppressed by the Glashow-Iliopoulos-Maiani (GIM) mechanism. Long-distance processes bring the predicted branching fractions up to the order of 10−23 and 10−13 for D0 → e+e− and D0 → μ+μ− decays, respectively [3]. These predictions are well below current experimental sensitivities. The lepton-flavor violating (LFV) decay D0 → e±μ∓ is forbidden in the SM. Several extensions of the SM predict D0 → ℓ+ℓ− branching fractions that are enhanced by several orders of magnitude compared with the SM expectations [1]. The connection between

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II. EVENT RECONSTRUCTION AND SELECTION

We form $D^0$ candidates by combining pairs of oppositely charged tracks and consider the following final states: $e^+e^-$, $\mu^+\mu^-$, $e^+\mu^-$, $\pi^+\pi^-$, and $K^-\pi^+$. We use the measured $D^0 \rightarrow \pi^+\pi^-$ yield and the known $D^0 \rightarrow \pi^+\pi^-$ branching fraction to normalize our $D^0 \rightarrow \ell^+\ell^-$ branching fractions. We also use the $D^0 \rightarrow \pi^+\pi^-$ candidates, as well as the $D^0 \rightarrow K^-\pi^+$ candidates, to measure the probability of misidentifying a $\pi$ as either a $\mu$ or an $e$. Combinatorial background is reduced by requiring that the $D^0$ candidate originate from the decay $D^*(2010)^+ \rightarrow D^0 \pi^+$ [6]. We select $D^0$ candidates produced in continuum $e^+e^- \rightarrow c\bar{c}$ events by requiring that the momentum of the $D^0$ candidate be above 2.4 GeV in the center-of-mass (CM) frame, which is close to the kinematic limit for $B \rightarrow D^+\pi$, $D^{*-} \rightarrow D^0\pi^-$. This reduces the combinatorial background from $e^+e^- \rightarrow BB$ events.

Backgrounds are estimated directly from data control samples. Signal $D^0$ candidates with a reconstructed $D^0$ mass above 1.9 GeV consist of random combinations of tracks. We use a sideband region above the signal region in the $D^0$ mass ([(1.90, 2.05) GeV] in a wide $\Delta m \equiv m(D^0 \pi^+) - m(D^0)$ window ([(0.141, 0.149) GeV]) to estimate the amount of combinatorial background. The $D^0$ and $\Delta m$ mass resolutions, measured in the $D^0\rightarrow\pi^+\pi^-$ sample, are 8.1 MeV and 0.2 MeV, respectively. We estimate the number of $D^0 \rightarrow \pi^+\pi^-$ background events selected as $D^0 \rightarrow \ell^+\ell^-$ candidates by scaling the observed $D^0 \rightarrow \pi^+\pi^-$ yield, with no particle identification criteria applied, by the product of pion misidentification probabilities and a misidentification correlation factor $G$. The misidentification correlation factor $G$ is estimated with the $D^0 \rightarrow K^-\pi^+$ data control sample.

The tracks for the $D^0$ candidates must have momenta greater than 0.1 GeV and have at least 6 hits in the SVT. The slow pion track from the $D^{*+} \rightarrow D^0\pi^+$ decay must have at least 12 position measurements in the DCH. A fit of the $D^{*-} \rightarrow D^0\pi^+$, $D^0 \rightarrow t^+t^-$ decay chain is performed where the $D^0$ tracks ($t$) are constrained to come from a common vertex and the $D^0$ and slow pion are constrained to form a common vertex within the beam interaction region. The $\chi^2$ probabilities of the $D^0$ and $D^*$ vertices from this fit must be at least 1%. The reconstructed $D^0$ mass $m(D^0)$ must be within $[1.65, 2.05]$ GeV and the mass difference $\Delta m$ must be within $[0.141, 0.149]$ GeV. We subtract a data-Monte-Carlo difference of 0.91 ± 0.06 MeV, measured in the $D^0 \rightarrow \pi^+\pi^-$ sample, from the reconstructed $D^0$ mass in the simulation.

We use an error-correcting output code (ECOC) algorithm [8] with 36 input variables to identify electrons and pions. The ECOC combines multiple bootstrap aggregated [8] decision tree [8] binary classifiers trained to separate $e, \pi, K,$ and $p$. The most important inputs for electron identification are the EMC energy divided by the track momentum, several EMC shower shape variables, and the deviation from the expected value divided by the measurement uncertainty for the Cherenkov angle and $dE/dx$ for the $e, \pi, K,$ and $p$ hypotheses. For tracks with momentum greater than 0.5 GeV, the electron identification has an efficiency of 95% for electrons and a pion misidentification probability of less than 0.2%. Neutral clusters in the EMC that are consistent with Bremsstrahlung radiation are used to correct the momentum and energy of electron candidates. The efficiency of the pion identification is above 90% for pions, with a kaon misidentification probability below 10%.

Muons are identified using a bootstrap aggregated decision tree algorithm with 30 input variables. Of these, the most important are the number and positions of the hits in the IFR, the difference between the measured and expected DCH $dE/dx$ for the muon hypothesis, and the energy deposited in the EMC. For tracks with momentum greater than 1 GeV, the muon identification has an efficiency of around 60% for muons, with a pion misidentification probability of between 0.5% and 1.5%.

The reconstruction efficiencies for the different channels after the above particle identification requirements are about 18% for $e^+e^-$, 9% for $\mu^+\mu^-$, 13% for $e^+\mu^-$, and 26% for $\pi^+\pi^-$. The background candidates that remain are either random combinations of two leptons (combinatorial background), or $D^0 \rightarrow \pi^+\pi^-$ decays where both pions pass the lepton identification criteria (peaking background). The $D^0 \rightarrow \pi^+\pi^-$ background is most important for the $D^0 \rightarrow \mu^+\mu^-$ channel.

Figure 1 shows the reconstructed invariant mass distributions from Monte Carlo (MC) simulated samples for the three $D^0 \rightarrow \ell^+\ell^-$ signal channels. Also shown are the distributions from $D^0 \rightarrow \pi^+\pi^-$ reconstructed as $D^0 \rightarrow \ell^+\ell^-$ and $D^0 \rightarrow K^-\pi^+$ reconstructed as $D^0 \rightarrow \ell^+\ell^-$ for each signal channel. The overlap between the $D^0 \rightarrow \ell^+\ell^-$ and $D^0 \rightarrow \pi^+\pi^-$ distributions is largest for the $D^0 \rightarrow \mu^+\mu^-$ channel, while the $D^0 \rightarrow \ell^+\ell^-$ and $D^0 \rightarrow K^-\pi^+$ distributions are well separated.

The combinatorial background originates mostly from events with two semileptonic $B$ and/or $D$ decays. The sample of events selected by the above criteria are dominantly from $e^+e^- \rightarrow BB$ events, rather than events from the $e^+e^- \rightarrow q\bar{q}$, $(q = u, d, s, c)$ continuum. We use a linear combination (Fisher discriminant 10) of the following five variables to reduce the combinatorial $BB$ background:

- The measured $D^0$ flight length divided by its uncertainty.
- The value of $|\cos\theta_{c\bar{c}}|$, where $\theta_{c\bar{c}}$ is defined as the angle between the momentum of the positively-charged $D^0$ daughter and the boost direction from the lab frame to the $D^0$ rest frame, all in the $D^0$ rest frame.
- The missing transverse momentum with respect to the beam axis.
The neutrinos from the semileptonic decays in the final state create missing transverse momentum in the CM frame. The ratio of the $D^0$ to $D^\ast$ and continuum background MC is used to separate signal events. The ratio of $D^0$ to $D^\ast$ and $D^0$ to $e^\pm\mu^\mp$ are similar to those of $D^0$ to $\mu^+\mu^-$.

The flight length for combinatorial background is symmetric about zero, while the signal has an exponential distribution. The $|\cos \theta_{hel}|$ distribution is uniform for signal but peaks at zero for combinatorial $B\bar{B}$ background. The neutrinos from the semileptonic decays in $B\bar{B}$ background events create missing transverse momentum, while there is none for signal events. The ratio of Fox-Wolfram moments uses general event-shape information to separate $B\bar{B}$ and continuum $q\bar{q}$ events. Finally, the signal has a broad $D^0$ CM momentum spectrum that peaks at around 3 GeV, while combinatorial background peaks at the minimum allowed value of 2.4 GeV.

The $D^0$ momentum in the CM frame.

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tent with the expectations from the Monte Carlo samples. However, the $D^0 \rightarrow e^+e^-$ sideband yield showed a substantial excess of events; 90 events were observed when $5.5 \pm 1.6$ were expected.

The excess of data sideband events over the expected background from Monte Carlo was investigated and found to have several distinct features: low track multiplicity, continuum-like event shape characteristics, tracks consistent with electrons produced in photon conversions, low $D^0$ daughter track momenta, and undetected energy along the beam axis. We found that such events result from hard initial state radiation events or two-photon interaction processes that are not simulated in the continuum MC samples used in the analysis. The following selection criteria were added in order to remove such background contributions:

- Events must have at least 5 tracks for the $D^0 \rightarrow e^+e^-$ channel and at least 4 tracks for the $D^0 \rightarrow \mu^+\mu^-$ and $D^0 \rightarrow e^+\mu^-$ channels.
- Events can have at most 3 electron candidates.
- The longitudinal boost of the event, reconstructed from all tracks and neutral clusters, along the high-energy beam direction $p_y/E$ in the CM frame must be greater than -0.5 for all three $D^0 \rightarrow \ell^+\ell^-$ channels.
- For $D^0 \rightarrow \mu^+\mu^-$ and $D^0 \rightarrow e^+\mu^-$ candidates, the pion track from the $D^{*+}$ decay and the leptons must be inconsistent with originating from a photon conversion.

The signal efficiencies for the $D^0 \rightarrow e^+e^-$, $D^0 \rightarrow \mu^+\mu^-$, and $D^0 \rightarrow e^+\mu^+$ channels for these additional criteria are 91.4%, 99.3%, and 96.8%, respectively. The $D^0 \rightarrow e^+e^-$ sideband yield in the data with these criteria applied is reduced to 8 events where $4.5 \pm 1.3$ are expected, based on the Monte Carlo samples.

A. Peaking $D^0 \rightarrow \pi^+\pi^-$ background estimation

The amount of $D^0 \rightarrow \pi^+\pi^-$ peaking background within the $m(D^0)$ signal window is estimated from data and calculated separately for each $D^0 \rightarrow \ell^+\ell^-$ channel using

$$N_{\pi\pi}^{BG} = \sum_i N_{\pi\pi,i}^{NP} \cdot \langle p_{f,i}^+ / p_{f,i}^- \rangle \cdot \epsilon_{m(D^0)} \cdot G$$  \hspace{1cm} (1)$$

where the sum $i$ is over the six data-taking periods, $N_{\pi\pi,i}^{NP}$ is the number of $D^0 \rightarrow \pi^+\pi^-$ events that pass all of the $D^0 \rightarrow \ell^+\ell^-$ selection criteria except for the lepton identification and $m(D^0)$ signal window requirements, $\langle p_{f,i}^+ / p_{f,i}^- \rangle$ is the product of the average probability that the $\pi^+$ and $\pi^-$ pass the lepton identification criteria, $\epsilon_{m(D^0)}$ is the efficiency for $D^0 \rightarrow \pi^+\pi^-$ background to satisfy the $m(D^0)$ signal window requirement, and $G$ takes into account a positive correlation in the probability that the $\pi^+$ and $\pi^-$ pass the muon identification criteria. The value of $\langle p_{f,i}^+ / p_{f,i}^- \rangle$ is measured using the ratio of the $D^0 \rightarrow \pi^+\pi^-$ yield requiring that the $\pi^+$ ($\pi^-$) satisfy the lepton identification requirements to the $D^0 \rightarrow \pi^+\pi^-$ yield with no lepton identification requirements applied. The $\langle p_{f,i}^+ / p_{f,i}^- \rangle$ vary between 0.5% and 1.5%. The probability that the $\pi^+$ and $\pi^-$ both pass the muon identification criteria is enhanced when the two tracks curve toward each other, instead of away from each other, in the plane perpendicular to the beam axis. We use $G = 1.19 \pm 0.05$ for the $D^0 \rightarrow \mu^+\mu^-$ channel and $G = 1$ for the $D^0 \rightarrow e^+e^-$ and $D^0 \rightarrow e^+\mu^+$ channels. The $G$ factor is measured using a high-statistics $D^0 \rightarrow K^-\pi^+$ sample where the $K$ is required to have a signature in the IFR that matches that of a $\pi$ which passes the $\mu$ identi-
fication criteria. This is in good agreement with the MC estimate of the $G$ factor value, 1.20 ± 0.10.

B. Combinatorial background estimation

The combinatorial background is estimated by using the number of observed events in a sideward region and the expected ratio of events $R_{cb}$ in the signal and sideward regions, determined from MC simulation. The sideward is above the signal region in the $D^0$ mass ([1.90, 2.05] GeV) in a wide $\Delta m$ window ([0.141, 0.149] GeV). We fit the $D^0$ mass and $\Delta m$ projections of the combinatorial background MC using 2nd-order polynomials. A two-dimensional probability density function (PDF) is formed by multiplying the one-dimensional PDFs, assuming the variables are uncorrelated. The combinatorial background signal-to-sideward ratio $R_{cb}$ is then computed from the ratio of the integrals of the two-dimensional PDF.

III. RESULTS

The distribution of $\Delta m$ vs $D^0$ mass as well as projections of $\Delta m$ and the $D^0$ mass for the data events for the three signal channels are shown in Fig. 4. Peaks from $D^0 \rightarrow K^-\pi^+$ and $D^0 \rightarrow \pi^+\pi^-$ are visible at 1.77 GeV and 1.85 GeV in the $D^0$ mass distribution for $D^0 \rightarrow \mu^+\mu^-$ candidates. We observe 1, 8, 2 events in the $D^0 \rightarrow e^+e^-$, $D^0 \rightarrow \mu^+\mu^-$, and $D^0 \rightarrow e^+\pi^-$ signal regions, respectively.

A. $D^0 \rightarrow \ell^+\ell^-$ Branching fractions

The yield of $D^0 \rightarrow \pi^+\pi^-$ decays in the $\pi\pi$ control sample, selected with the same $F$ and $|\cos\theta_{hel}|$ criteria for each $D^0 \rightarrow \ell^+\ell^-$ signal mode (see Table 1), is used to normalize the $D^0 \rightarrow \ell^+\ell^-$ signal branching fraction. For each $D^0 \rightarrow \ell^+\ell^-$ signal channel, the $D^0 \rightarrow \pi^+\pi^-$ yield $N_{\pi\pi}^{fit}$ is determined by fitting the $D^0$ mass spectrum of the $D^0 \rightarrow \pi^+\pi^-$ control sample in the range [1.7, 2.0] GeV. The fit has three components: $D^0 \rightarrow \pi^+\pi^-$, $D^0 \rightarrow K^-\pi^+$, and combinatorial background. The PDF for the $D^0 \rightarrow \pi^+\pi^-$ component is the sum of a Crystal Ball function and two Gaussians. The Crystal Ball function is a Gaussian modified to have an extended, power-law tail on the low side [12]. The PDF for the $D^0 \rightarrow K^-\pi^+$ component is the sum of a Crystal Ball function and an exponential function. The combinatorial background PDF is an exponential function.

The $D^0 \rightarrow \ell^+\ell^-$ branching fraction is given by

$$B_{\ell\ell} = \left(\frac{N_{\ell\ell}}{N_{\pi\pi}^{fit}}\right) \frac{\epsilon_{\pi\pi}}{\epsilon_{\ell\ell}} B_{\pi\pi} = S_{\ell\ell} \cdot N_{\ell\ell} \quad (2)$$

where $N_{\ell\ell}$ is the number of $D^0 \rightarrow \ell^+\ell^-$ signal candidates, $N_{\pi\pi}^{fit}$ is the number of $D^0 \rightarrow \pi^+\pi^-$ candidates from the fit, $\epsilon_{\pi\pi}$ and $\epsilon_{\ell\ell}$ are the efficiencies for the corresponding decay modes, $B_{\pi\pi} = (1.400 \pm 0.026) \times 10^{-3}$ is the $D^0 \rightarrow \pi^+\pi^-$ branching fraction [13], and $S_{\ell\ell}$ is defined by

$$S_{\ell\ell} = \frac{B_{\pi\pi}}{N_{\pi\pi}^{fit} \epsilon_{\ell\ell}} \quad (3)$$

The expected observed number of events in the signal region is given by

$$N_{obs} = B_{\ell\ell} / S_{\ell\ell} + N_{BG} \quad (4)$$

The uncertainties on $S_{\ell\ell}$ and $N_{BG}$ are incorporated into a likelihood function by convolving a Poisson PDF in $N_{obs}$ with Gaussian PDFs in $S_{\ell\ell}$ and $N_{BG}$. We determine 90% confidence level intervals using the likelihood ratio ordering principle of Feldman and Cousins [14] to construct the confidence belts. The estimated branching fractions and one standard deviation uncertainties are determined from the values of $B_{\ell\ell}$ that maximize the likelihood and give a change of 0.5 in the log likelihood relative to the maximum, respectively.

B. Systematic uncertainties

Table 1 summarizes the systematic uncertainties. Several of the uncertainties in $\epsilon_{\pi\pi}/\epsilon_{\ell\ell}$ cancel, including tracking efficiency for the $D^0$ daughters, slow pion efficiency, and the efficiencies of the $F$ and $D^0$ momentum requirements. The uncertainty on $\epsilon_{\pi\pi}/\epsilon_{\ell\ell}$ due to particle identification is 4%. Bremsstrahlung creates a low-side tail in the $D^0$ mass distributions for the $D^0 \rightarrow e^+e^-$ and $D^0 \rightarrow e^+\mu^+$ decay modes. The uncertainty $\epsilon_{\ell\ell}$ due to the modeling of this tail is 3% for $D^0 \rightarrow e^+e^-$ and 2% for $D^0 \rightarrow e^+\mu^+$. The Crystal Ball shape parameters that describe the low-side tail of the $D^0$ mass distribution were varied, leading to an uncertainty of 1.1% to 1.3% on $N_{\pi\pi}^{fit}$. We use the world average for the $D^0 \rightarrow \pi^+\pi^-$ branching fraction [13], which has an uncertainty of 1.9%. We combine the above relative uncertainties in quadrature resulting in 4.6% to 5.4% systematic uncertainties on $S_{\ell\ell}$.

The $D^0$ mass range for the fit used to determine the combinatorial background PDF was varied from [1.70, 2.05] GeV to [1.80, 2.05] GeV. The difference in the resulting signal-to-sideward ratio $R_{cb}$ is taken as a systematic uncertainty. The pion misidentification probabilities for $e$ and $\mu$ measured in data are in good agreement with the MC simulation. We use the larger of either the difference between the data and the MC or the statistical uncertainty on the MC misidentification probabilities as a systematic uncertainty. For the $D^0 \rightarrow \mu^+\mu^-$ decay mode, we take the uncertainty on the MC estimate for the $G$ factor of 8% as a systematic uncertainty on the $G$ estimate from the $D^0 \rightarrow K^-\pi^+$ data control sample.
C. Branching Fraction Results

Table III presents the results, where \(N_{SB}\) is the number of events in the upper sideband, \(N_{cb}\) is the expected number of combinatorial background events in the signal window, \(N_{BG}\) is the number of events from the \(D^0 \to \pi^+\pi^-\) peaking background, and \(N_{BG}\) (data) is the expected number of total background events in the data.

For the \(D^0 \to e^+e^-\) and \(D^0 \to e^+\mu^+\) channels, the event yield in the signal region is consistent with background only. We observe 1 and 2 events with expected backgrounds of \(1.0 \pm 0.5\) and \(1.4 \pm 0.3\) events for the \(D^0 \to e^+e^-\) and \(D^0 \to e^+\mu^+\) channels, respectively. The 90% confidence interval upper limits for the branching fractions are \(< 1.7 \times 10^{-7}\) for \(D^0 \to e^+e^-\) and \(< 3.3 \times 10^{-7}\) for \(D^0 \to e^+\mu^+\).

For the \(D^0 \to \mu^+\mu^-\) channel, we observe 8 events in the signal region, where we expect \(3.9 \pm 0.6\) background events. There is a cluster of of \(D^0 \to \mu^+\mu^-\) candidate events in Fig. 4 just above and below the lower \(D^0\) mass edge of the signal region, where the \(D^0 \to \pi^+\pi^-\) background is expected. We expect \(7.5 \pm 0.8\) \(D^0 \to \pi^+\pi^-\) events in the entire [1.7, 2.05] GeV \(D^0\) mass range, with 93% of these events falling within the narrower [1.830,1.875] GeV range. The combinatorial background in the [1.830,1.875] GeV \(D^0\) mass interval is expected to be \(1.8 \pm 0.6\) events, giving a total expected background of \(8.8 \pm 1.1\) events. In this interval,
we observe 15 events. The probability of observing 15 or more events when 8.8 ± 1.1 events are expected is 4.6%, which corresponds to a 1.7 standard deviation upward fluctuation from the mean for a Gaussian distribution (i.e., (1.7/√2) + 1/2 = 1.0 ± 0.046). The probability of observing 8 events when 3.9 ± 0.6 events are expected is 5.4%. We conclude that the excess over the expected background is not statistically significant. The Feldman-Cousins method results in a two-sided 90% confidence interval for the $D^0 \rightarrow \mu^+\mu^-$ branching fraction of $[0.6, 8.1] \times 10^{-7}$.

In summary, we have searched for the leptonic charm decays $D^0 \rightarrow e^+e^-$, $D^0 \rightarrow \mu^+\mu^-$, and $D^0 \rightarrow e^\pm \mu^\mp$ using 468 fb$^{-1}$ of integrated luminosity recorded by the BaBar experiment. We find no statistically significant excess over the expected background. These results supersede our previous results [15] and are consistent with the results of the Belle experiment [16], which has set 90% confidence level upper limits of $< 0.79 \times 10^{-7}$, $< 1.4 \times 10^{-7}$, and $< 2.6 \times 10^{-7}$, for the $D^0 \rightarrow e^+e^-$, $D^0 \rightarrow \mu^+\mu^-$, and $D^0 \rightarrow e^\pm \mu^\mp$ branching fractions, respectively. The LHCb experiment has recently presented preliminary search results [17] for $D^0 \rightarrow \mu^+\mu^-$, where they find no evidence for this decay and set an upper limit on the branching fraction of $< 1.3 \times 10^{-8}$ at 95% C.L.

**TABLE II:** Systematic uncertainties. The uncertainty on $S_{\ell\ell}$ results from the uncertainties on $\epsilon_{\pi\pi}/\epsilon_{\ell\ell}$, $N_{\pi\pi}^{cb}$, and $B_{\pi\pi}$ added in quadrature. The systematic uncertainty on the overall background $N_{BG}$ is obtained from the uncertainties on $N_{SS}^{cb}$ and $N_{cb}$ added in quadrature.

| Source | $D^0 \rightarrow e^+e^-$ | $D^0 \rightarrow \mu^+\mu^-$ | $D^0 \rightarrow e^\pm \mu^\mp$ |
|--------|--------------------------|-----------------------------|-----------------------------|
| $\epsilon_{\pi\pi}/\epsilon_{\ell\ell}$, particle ID | 4% | 4% | 4% |
| $\epsilon_{\pi\pi}/\epsilon_{\ell\ell}$, Bremsstrahlung | 3% | — | 2% |
| $N_{\pi\pi}^{cb}$ | 1.2% | 1.3% | 1.1% |
| $B_{\pi\pi}$ | 1.9% | 1.9% | 1.9% |
| $S_{\ell\ell}$ | 5.4% | 4.6% | 5.0% |
| $N_{BG}$ | 11% (0.004 events) | 16% (0.43 events) | 5% (0.02 events) |
| $N_{cb}, R_{cb}$ | 36% (0.35 events) | 20% (0.25 events) | 19% (0.20 events) |
| $N_{BG}$ | 0.35 events | 0.50 events | 0.20 events |

**TABLE III:** Results for the observed event yields ($N_{\text{obs}}$), estimated background ($N_{BG}$), and signal branching fractions ($B_{\ell\ell}$). The first uncertainty is statistical and the second systematic. $N_{SS}$ is the observed number of events in the sideband, $R_{cb}$ is the signal-to-sideband ratio for combinatorial background, $N_{cb}$ and $N_{\pi\pi}^{BG}$ are the estimated combinatorial and $D^0 \rightarrow \pi^+\pi^-$ backgrounds in the signal region, $N_{\pi\pi}^{cb}$ is the fitted yield in the $D^0 \rightarrow \pi^+\pi^-$ control sample, $\epsilon_{\pi\pi}$ and $\epsilon_{\ell\ell}$ are the $\pi\pi$ control sample and signal selection efficiencies, determined from Monte Carlo samples, which have negligible statistical uncertainties. The systematic uncertainty on $\epsilon_{\pi\pi}/\epsilon_{\ell\ell}$ is included in the systematic uncertainty on $S_{\ell\ell}$, which is defined in Eqn. [7].

| Source | $D^0 \rightarrow e^+e^-$ | $D^0 \rightarrow \mu^+\mu^-$ | $D^0 \rightarrow e^\pm \mu^\mp$ |
|--------|--------------------------|-----------------------------|-----------------------------|
| $N_{SS}$ | 8 | 27 | 24 |
| $R_{cb}$ | 0.121 ± 0.023 ± 0.044 | 0.046 ± 0.005 ± 0.009 | 0.042 ± 0.006 ± 0.008 |
| $N_{cb}$ | 0.97 ± 0.39 ± 0.35 | 1.24 ± 0.27 ± 0.25 | 1.00 ± 0.25 ± 0.20 |
| $N_{\pi\pi}^{BG}$ | 0.037 ± 0.012 ± 0.004 | 2.64 ± 0.22 ± 0.43 | 0.42 ± 0.08 ± 0.02 |
| $N_{BG}$ | 1.01 ± 0.39 ± 0.35 | 3.88 ± 0.35 ± 0.50 | 1.42 ± 0.26 ± 0.20 |
| $N_{\pi\pi}^{cb}$ | 39930 ± 210 ± 490 | 51800 ± 240 ± 660 | 39840 ± 210 ± 430 |
| $\epsilon_{\pi\pi}$ | 14.4% | 18.7% | 14.6% |
| $\epsilon_{\ell\ell}$ | 9.48% | 6.29% | 6.97% |
| $S_{\ell\ell}$ ($\times 10^{-9}$) | 53.4 ± 0.2 ± 2.9 | 80.6 ± 0.4 ± 3.7 | 73.9 ± 0.4 ± 3.7 |
| $N_{\text{obs}}$ | 1 | 8 | 2 |
| $B_{\ell\ell}$ ($\times 10^{-9}$) | 0.1 $^{+0.7}_{-0.4}$ | 3.3 $^{+2.6}_{-2.0}$ | 0.5 $^{+1.3}_{-0.9}$ |
| $B_{\ell\ell}$ ($\times 10^{-7}$) 90% C.L. | < 1.7 | [0.6, 8.1] | < 3.3 |
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