Impact of grain size distributions on the dust enrichment in high-redshift quasars

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ABSTRACT

In high-redshift ($z > 5$) quasars, a large amount of dust ($\sim 10^8 \, M_\odot$) has been observed. In order to explain the large dust content, we focus on a possibility that grain growth by the accretion of heavy elements is the dominant dust source. We adopt a chemical evolution model applicable to nearby galaxies, but utilize parameters adequate to high-$z$ quasars. It is assumed that metals and dust are predominantly ejected by Type II supernovae (SNe). We have found that grain growth strongly depends on the grain size distribution. If we simply use the size distribution of grains ejected from SNe, grain growth is inefficient because of the lack of small grains (i.e. small surface-to-volume ratio of the dust grains). However, if we take small grain production by interstellar shattering into consideration, grain growth is efficient enough to account for the rich dust abundance in high-$z$ quasars. Our results not only confirm that grain growth is necessary to explain the large amount of dust in high-$z$ quasars, but also demonstrate that grain size distributions have a critical impact on grain growth.

Key words: ISM: clouds – dust, extinction – galaxies: evolution – galaxies: high-redshift – galaxies: ISM – quasars: general.

1 INTRODUCTION

The origin of dust grains in the Universe is one of the fundamental problems in astrophysics. It is widely believed that the evolution of dust content in galaxies is influenced by dust formation in stellar ejecta, dust destruction in supernova (SN) remnants and grain growth by the accretion of metals on to the pre-existing dust grains in molecular clouds (e.g. Dwek 1998). Various authors have shown that grain growth in molecular clouds dominates the increase of dust mass in nearby galaxies (Hirashita 1999; Inoue 2003; Zhukovska, Gail & Trieloff 2008; Draine 2009; Inoue 2011). Zhukovska et al. (2008) also mention that grain growth depends on the mean surface-to-volume ratio of the dust grains. In our previous work (Hirashita & Kuo 2011, hereafter HK11), we have investigated the effects of dust grain size distribution on grain growth and found that the grain size distribution has a large influence on the efficiency of grain growth because the surface-to-volume ratio is governed by the grain size distribution.

The extinction curves in the Galaxy and the Magellanic Clouds can be explained with dust grain size distributions $n(a) \propto a^{-3.5}$, where $a$ is the grain radius and $n(a) \, da$ is the number density of grains whose radius is between $a$ and $a + da$ (Mathis, Rumpl & Nordsieck 1977; Pei 1992). However, high-redshift quasars exhibit different extinction curves from the ones in local galaxies (e.g. Gall, Andersen & Hjorth 2011), which may indicate different grain size distributions. Different dust sources and/or different grain processing in the early Universe may be the reason for the different extinction curves in high-$z$ quasars. In the early Universe, Type II supernovae (simply denoted as SNe in this Letter) should be the foremost source of dust formation because of the short lifetimes of the progenitors (Gall, Andersen & Hjorth 2011), albeit asymptotic giant branch (AGB) stars may have contribution even at $z > 5$ for some stellar initial mass function (Valiante et al. 2009). Star-forming regions may also host significant grain processing such as shattering (Hirashita et al. 2010).

Grain growth in molecular clouds may dominate the grain mass increase not only in the local Universe, but also at high $z$ (Mattsson 2011; Pipino et al. 2011; Valiante et al. 2011; Asano et al. 2012). However, the potential importance of dust grain size distributions in grain growth has not been focused on. As emphasized above, the grain size distributions in high-$z$ quasars should be different from those in local galaxies. Therefore, we should reconsider grain growth by using grain size distributions applicable to high-$z$ systems.

Size distributions of grains produced and ejected from SNe (called SN-dust) are calculated by Nozawa et al. (2007), who take dust condensation and destruction in SNe into account. They show that the average grain size of SN-dust is biased to large sizes because small grains are efficiently trapped in the shocked region and

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considerably destroyed by thermal sputtering. This means that the grain size distribution is completely different from the local 3.5 law and that the surface-to-volume ratio is smaller than the local one. As a result, we have to re-examine whether grain growth is efficient enough to explain the large dust abundance in high-z quasars.

After SN-dust is injected into the interstellar medium (ISM), the grain size distribution can be modified. Dust grains acquire large velocity dispersions in a warm ionized medium through dynamical coupling with turbulent motion (Yan, Lazarian & Draine 2004). Grain–grain collisions at velocities driven by turbulence lead to efficient shattering, which produces a large number of small grains (Hirashita et al. 2010). The extinction curve observed in a high-z quasar by Maiolino et al. (2004) is also reproduced by a grain size distribution after shattering (Hirashita et al. 2010). Shattering raises the surface-to-volume ratio, leading to a higher grain growth rate.

In this Letter, we examine the significance of grain size distribution on grain growth in high-z quasars by focusing on two different grain size distributions as representative ones expected theoretically in high-z quasars: one is the grain size distribution of SN-dust (Nozawa et al. 2007) and the other is the size distribution of grains processed by interstellar shattering (Hirashita et al. 2010). This Letter is organized as follows. In Section 2, we explain theoretical models of dust enrichment, focusing on grain growth by accretion. In Section 3, we show the results, which we discuss in more general contexts in Section 4. Finally, Section 5 gives the conclusion.

2 MODEL

2.1 Dust enrichment

We adopt a chemical evolution model that describes the time evolution of gas, metals and dust in a galaxy. In order to focus on the effect of grain size distribution on grain growth, we adopt a simple model, which has already been shown to be applicable to nearby galaxies (Hirashita 1999; HK11), but use parameter values suitable for high-z (z > 5) quasars. We neglect inflow and outflow, and treat the system as a closed box.1 The abundances of dust and metals are tightly related, so the model equations are finally reduced to the relation between dust-to-gas ratio and metallicity by adopting the instantaneous recycling approximation (HK11), which can be applied as long as we consider time-scales longer than the lifetime of massive stars:

\[ \frac{dY_X}{dt} = f_{in,X}(RZ_X + Y_X) - (\beta_{SN} + R)D_X \]

\[ + \frac{1}{\psi} \left[ \frac{dM_{dust,X}}{dr} \right]_{acc}, \]

(1)

where \( Z_X \) is the mass abundance of element X (X is a key element of a dust species; X = Si for silicate and X = C for carbonaceous grains) in both gas and dust phases, D_X is the mass abundance of a dust species whose key element is X, \( R \) is the return fraction of the mass from stars formed, \( Y_X \) is the mass fraction of element X that is newly produced and ejected by stars, \( f_{in,X} \) is the dust condensation efficiency of the element X in the ejecta, \( \psi \) is the star formation rate, \( \beta_{SN} \) is the destruction efficiency of dust by SN shocks (defined below) and \( [dM_{dust,X}/dt]_{acc} \) is the increasing rate of dust mass by accretion. The destruction efficiency by SN shock was introduced by McKee (1989) as \( \beta_{SN} \equiv \epsilon_{SN}M/g, \) where \( \epsilon_{SN} \) is the fraction of dust destroyed in a single SN blast, \( M \) is the gas mass swept per SN blast and \( g \) is the SN rate. We adopt \( \beta_{SN} = 9.65 \) (HK11). In deriving equation (1), some quantities are eliminated. The gas mass is used to normalize the metal and dust masses to obtain \( Z_X \) and \( D_X \), respectively, and thus acts as a normalizing factor in our formulation. The star formation time-scale is also eliminated: changing the star formation time-scale just varies the quickness of metal and dust enrichment, leaving the relation between \( Z_X \) and \( D_X \) unchanged. We refer to HK11 for the derivation of equation (1). We assume \( D_X = 0 \) at \( Z_X = 0 \).

2.2 Grain growth by accretion

In HK11, we have formulated the grain growth by accretion considering the dependence on the grain size distribution. We also assume that the molecular clouds host both grain growth and star formation. Then, we obtain (HK11)

\[ \left[ \frac{dM_{dust,X}}{dr} \right]_{acc} = \frac{\beta_X D_X \psi}{\epsilon}, \]

(2)

where \( \beta_X \) is the mass increment of dust whose key species is X and \( \epsilon \) is the star formation efficiency in a single molecular cloud. By assuming that grain growth is governed by the sticking of the key element X (i.e. Si for silicate and C for carbonaceous dust), HK11 derived the following formula for \( \beta_X \):

\[ \beta_X \sim \left( \frac{(a^{3/2})_0}{3y(a^{2})_0 + 3y^2(a_0) + y^3} + \frac{1}{\xi_X} \right)^{-1}, \]

(3)

where \( y \equiv a_0 \rho_X \tau_{el} / \tau \) \( [a_0 = 0.1 \mu m] \) is a typical grain radius, \( \tau_{el} \) is the lifetime of molecular clouds and \( \tau \propto a_0 \) is the grain growth time-scale given below in equation (4); note that \( a_0 \) cancels out in obtaining \( y \) so that we can take an arbitrary value for \( a_0 \). \( (a^{3/2})_0 \) is the average of \( \langle a^{3/2} \rangle (\ell = 1, 2 \) and 3) weighted for the grain size distribution (i.e. moments) and \( \xi_X = 1 - f_X D_X/Z_X \) is the fraction of element X in gas phase \( (f_X = \text{mass fraction of element X contained in the grains}) \). The grain growth time-scale \( \tau \) is given by

\[ \tau \equiv a_0 \left/ \left( m_X \frac{S_X}{f_{SG}} \left( \frac{Z_X}{Z_X(\infty)} \right) \left( \frac{X}{H} \right) \frac{n_H}{2 \pi m_H k_B T_{gas}} \right)^{1/2} \right. \],

(4)

where \( n_H \) is the number density of hydrogen nuclei in the molecular clouds, \( (X/H)(\infty) \) is the solar abundance of element X relative to hydrogen in number, \( S_X \) is the material density of a dust grain whose key species is X, \( S_X(\infty) \) is the sticking probability of element X onto the dust, \( m_X \) is the atomic mass of element X, \( T_{gas} \) is the gas temperature in the molecular clouds and \( k_B \) is the Boltzmann constant. By using equation (2), equation (1) can be rewritten as

\[ \frac{dY_X}{dt} = f_{in,X}(RZ_X + Y_X) - \frac{\beta_{SN} + R - \beta_X/\epsilon}{\psi}D_X, \]

(5)

2.3 Grain size distribution

We assume that the dust and metals are predominantly supplied from SNe in high-z (z > 5) quasars because they are the first significant dust source (Section 1). Although AGB stars may contribute to the dust enrichment even at z > 5, our conclusion in this Letter is not altered as long as AGB stars supply large (~0.1 µm) grains as suggested by observations (Groenewegen 1997; Gauger et al. 1999).
expected to raise the grain growth efficiency. We adopt the grain size distribution after shattering from Hirashita et al. (2010); the solar-metallicity case with hydrogen number density \( n_H = 1 \text{ cm}^{-3} \) and shattering duration \( t = 5 \text{ Myr} \). This case is called ‘grain size distribution with shattering’. Although it is difficult to constrain \( t \) and \( n_H \) from observations, this single case is sufficient to demonstrate the importance of the change of grain size distribution by shattering. Since we only focus on grain growth around \( Z \gtrsim Z_\odot \), the assumption of solar metallicity is reasonable in this Letter.

The above two grain size distributions adopted are shown in Fig. 1 for silicate and carbonaceous species. The moments of grain radii \((a^{'0}_j)\) necessary to estimate \( \beta_X \) in equation (3) are listed in Table 1. We observe that shattering makes the typical grain size smaller. We fix \((a^{'0}_i)\); in other words, we fix the grain size distribution throughout the galaxy evolution to focus on the effects of grain size distribution on grain growth.

2.4 Selection of parameter values

The typical time-scale of grain growth in equation (4) is estimated as (HK11)
\[
\tau = 6.30 \times 10^3 a_{0.1}^{-1} (Z_{Si}/Z_{Si,\odot})^{-1} n_H^{-1} T_{S0}^{-1/2} S_{0.3}^{-1} \text{ yr} \quad (6)
\]
for silicate, and as
\[
\tau = 5.59 \times 10^7 a_{0.1}^{-1} (Z_{C}/Z_{C,\odot})^{-1} n_H^{-1} T_{S0}^{-1/2} S_{0.3}^{-1} \text{ yr} \quad (7)
\]
for carbonaceous species, where \( a_{0.1} \equiv a/0.1 \mu m \), \( n_H = n_H/10^{3} \text{ cm}^{-3} \), \( T_{S0} = T_{gas}/50 \text{ K} \) and \( S_{0.3} \equiv S_X/0.3 \). We adopt the same values as those of HK11 (see also the references therein): \( n_H = 10^{3} \text{ cm}^{-3} \), \( T_{gas} = 50 \text{ K} \) and \( S_X = 0.3 \). For the solar abundance of Si and C, we adopt \((X/H)_{\odot}\) listed in Table 2, and convert it to \( Z_X \) by \( Z_X = (m_X/m_H)(X/H) \) \((\mu = 1.4 \text{ is the correction for helium})
We adopt \( X, f_X, m_X, (X/H)_{\odot} \) and \( \rho_X \) following HK11 (listed in Table 2). As a metallicity indicator, we adopt the oxygen abundance \((O/H)\), whose solar value is assumed to be 12 + \( \log(O/H) \) = 8.76 (Lodders 2003). The abundance of X is converted to that of O by assuming the abundance pattern calculated by the 20 M\( \odot \) SN model by Umeda & Nomoto (2002); the ejected masses of O, C and Si are 1.56, 0.257 and 0.257 M\( \odot \), respectively.

In the SN model adopted (Umeda & Nomoto 2002; Nozawa et al. 2007), \( R = 8.87 \times 10^{-2}, Z_{Si} = 9.22 \times 10^{-4}, Z_{C} = 1.71 \times 10^{-3}, f_{Si,Si} = 0.351 \) and \( f_{Si,C} = 0.135 \). Besides, for the lifetime of a molecular cloud, we adopt \( \tau_{S0} = 10^{3} \text{ yr} \) (e.g. Fukui & Kawamura 2010), but we also mention a possibility of a longer lifetime in Section 4.2.

3 RESULTS

3.1 Without shattering

We examine the relation between dust-to-gas ratio and metallicity for the grain size distribution without shattering. The result is exhibited in Fig. 2(a). At low metallicities \([12+\log(O/H) < 8.5]\), the dust is simply supplied from SNe, which leads to an

Table 1. Moments.

|                  | Silicate | Carbonaceous |
|------------------|----------|--------------|
|                  | \(a^0_0\) (\(\mu m\)) | \(a^0_0\) (\(\mu m\)) | \(a^0_0\) (\(\mu m\)) | \(a^0_0\) (\(\mu m\)) | \(a^0_0\) (\(\mu m\)) | \(a^0_0\) (\(\mu m\)) |
| Nozawa et al. (2007) | 2.32 \times 10^{-2} | 1.95 \times 10^{-3} | 4.83 \times 10^{-4} | 8.59 \times 10^{-3} | 3.45 \times 10^{-4} | 6.35 \times 10^{-5} |
| Hirashita et al. (2010) | 7.84 \times 10^{-4} | 3.23 \times 10^{-6} | 4.35 \times 10^{-7} | 5.42 \times 10^{-4} | 5.56 \times 10^{-7} | 1.60 \times 10^{-8} |
approximately linear increase of the dust-to-gas ratio in terms of the metallicity. When $D_X$ reaches $\sim f_{\text{m,}X} \Gamma_X / \beta_{\text{SN}}$ ($\sim 3 \times 10^5$ and $2 \times 10^{-3}$ for silicate and carbonaceous dust, respectively), the dust destruction becomes comparable to the dust supply from SNe (equation 5). Thus, the increase of the dust-to-gas ratio saturates around $12 + \log (O/H) \simeq 8.5$. Around $12 + \log (O/H) \sim 9$ ($\sim 2 Z_\odot$) the dust-to-gas ratio rapidly increases because of the non-linearity of grain growth ($d D_X / d Z_X \propto D_X Z_X$; that is, grain growth occurs as a result of collisions between dust grains and metals) in molecular clouds. As shown in HK11, the grain growth becomes prominent at a certain critical metallicity depending on dust grain size distribution (see Section 4.1). Under the size distribution without shattering, dust growth becomes prominent only after the metallicity reaches a supersolar value. This is because of inefficient grain growth caused by the large surface-to-volume ratio of dust grains.

In addition, SNe produce a larger amount of silicate than carbonaceous dust. After grain growth in molecular clouds, the silicate species is still dominant over the carbonaceous species.

### 3.2 With shattering

If we adopt the grain size distribution with shattering, we obtain the result exhibited in Fig. 2(b). Compared with the case in the previous subsection, the rapid increase of dust-to-gas ratio occurs at a lower metallicity, $12 + \log (O/H) \simeq 8.3$ ($\gtrsim 1/3 Z_\odot$), because shattering remarkably raises the surface-to-volume ratio of the dust grains.

### 3.3 Observational data

Michałowski et al. (2010) have estimated the dust and gas mass by using the millimetre continuum and CO lines, respectively, for nine $z > 5$ quasars. Their samples show high dust-to-gas ratios from $1.65 \times 10^{-2}$ to $4.30 \times 10^{-2}$, which could be regarded as upper limits because they did not take neutral hydrogen into account. If we alternatively utilize their dynamical mass as an upper limit for the gas mass, we then obtain $D > 8.0 \times 10^{-4}$ (assuming an inclination angle of $40^\circ$) to be a lower limit of the dust-to-gas ratio. Juarez et al. (2009) claim that high-$z$ ($z > 5$) quasars are likely to have supersolar metallicities ($\gtrsim 7 Z_\odot$) based on observations of broad-line regions. Narrow-line regions (NLRs) may trace the metal content of the entire quasi-stellar object (QSO) better, and Matsuoka et al. (2009) indicate that the NLRs in quasars at $1 \lesssim z \lesssim 4$ have solar metallicities. Considering that the bright QSOs at $z > 5$ are highly biased to the most luminous and metal-enriched systems, it is reasonable to assume that the metallicities of $z > 5$ QSOs is $\gtrsim Z_\odot$. Comparing our results with the observational lower limit of dust-to-gas ratio (Fig. 2), we find that at least $12 + \log (O/H) = 9.2$ ($Z \sim 3 Z_\odot$) is required to explain the lower limit of dust-to-gas ratio if we adopt the grain size distribution without shattering. Thus, a supersolar metallicity is strongly required to explain the rich dust content in high-redshift quasars. With shattering, however, the dust-to-gas ratio reaches the observational lower limit at a more moderate metallicity [$12 + \log (O/H) = 8.6; Z \sim 0.7 Z_\odot$] because of the grain growth at a lower metallicity.

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**Figure 2.** Relation between dust-to-gas ratio and metallicity. The solid lines show the total dust-to-gas ratio. The dotted and dashed lines present the contributions from silicate and carbonaceous dust, respectively. The horizontal dot-dashed line show the lower limit for the dust-to-gas ratio in the high-$z$ quasar sample in Michałowski et al. (2010). Panels (a) and (b) present the results for the grain size distribution without and with shattering, respectively, along with triangles marking the critical metallicities for grain growth. Panel (c) shows the result for a high density ($\rho_H = 10^3$ cm$^{-3}$).
4 DISCUSSION

4.1 Critical metallicity for grain growth

Inoue (2011) and Asano et al. (2012) have shown that the grain growth by accretion dominates the grain abundance if the metallicity is larger than a certain critical metallicity. According to equation (4), the hydrogen number density in molecular clouds, $n_H$, is also an important quantity that determines the timescale of grain growth, $\tau$. We have presumed that $n_H = 10^3$ cm$^{-3}$. However, in some environments such as circumnuclear starburst regions in high-$z$ quasars, the physical conditions of molecular clouds can be quite different. Some recent observations imply that the density in molecular clouds in high-$z$ quasars is higher than that in nearby galaxies (Gao et al. 2007; Klessen, Spaans, & Jappsen 2007; Riechers et al. 2007). In order to investigate a possibility of a larger $n_H$, we adopt $n_H = 10^4$ cm$^{-3}$. In Fig. 2(c), we show the result for the dust grain size distribution without shattering. We observe that higher gas density enhances grain growth and that the rapid increase of dust-to-gas ratio occurs at a lower metallicity. Therefore, the grain size distribution without shattering can be reconciled with the observed dust-to-gas ratio in high-$z$ quasars if we assume such a high density as $n_H \gtrsim 10^4$ cm$^{-3}$.

Equation (3) offers another possibility of enhancing grain growth. The dust mass increment $\beta_X$ is a function of $\tau_d/\tau$. As a result, a longer lifetime of molecular clouds hosting the grain growth $\tau_d$ has the same effect as a shorter typical time-scale of grain growth $\tau$, which means that $\tau_d = 10^3$ yr instead of $\tau_d = 10^4$ yr has the same effect as applying $n_H = 10^3$ cm$^{-3}$ instead of $n_H = 10^4$ cm$^{-3}$. Koda et al. (2009) have indicated that the presence of sheared structure within the spiral arms in the Milky Way supports a lifetime of molecular clouds comparable to galactic rotational time-scales ($\sim 10^9$ yr). Moreover, the gas temperature $T_{\text{gas}}$ and the sticking probability $S_X$ also enter the timescale (see equations 6 and 7); however, since $T_{\text{gas}}$ and $S_X$ cannot be much larger than the adopted values, it is difficult to make $\tau$ shorter by changing $T_{\text{gas}}$ or $S_X$.

5 CONCLUSION

The importance of grain size distribution on dust enrichment in high-redshift ($z > 5$) quasars has been investigated in this work. We have found that, if the grain size distribution of SN-dust is considered, very high metallicity ($\gtrsim 3 Z_{\odot}$) is required to explain the dust-to-gas ratio of those quasars under similar quantities to the local molecular clouds ($n_H = 10^3$ cm$^{-3}$ and $\tau_d = 10^3$ yr). However, if small grains are produced by shattering, grain growth is activated and the dust-to-gas ratio in high-$z$ quasars can be explained by more moderate metallicities ($\gtrsim 0.7 Z_{\odot}$). Thus, we conclude that the dust grain size distribution has a dramatic impact on the evolution of dust content in high-$z$ quasars.

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