Imprint of a scalar era on the primordial spectrum of gravitational waves

Francesco D’Eramo\textsuperscript{1,2} and Kai Schmitz\textsuperscript{1,2}

\textsuperscript{1} Dipartimento di Fisica e Astronomia, Università degli Studi di Padova, Via Marzolo 8, 35131 Padova, Italy
\textsuperscript{2} Istituto Nazionale di Fisica Nucleare (INFN), Sezione di Padova, Via Marzolo 8, 35131 Padova, Italy

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Upcoming searches for the stochastic background of inflationary gravitational waves (GWs) offer the exciting possibility to probe the evolution of our Universe prior to Big Bang nucleosynthesis. In this spirit, we explore the sensitivity of future GW observations to a broad class of beyond-the-Standard-Model scenarios that lead to a nonstandard expansion history. We consider a new scalar field whose coherent oscillations dominate the energy density of the Universe at very early times, resulting in a scalar era prior to the standard radiation-dominated era. The imprint of this scalar era on the primordial GW spectrum provides a means to probe well-motivated yet elusive models of particle physics. Our work highlights the complementarity of future GW observatories across the entire range of accessible frequencies.

Introduction. The detection of gravitational waves (GWs) \cite{LIGO_Virgo} by LIGO \cite{LIGO1, LIGO2} and Virgo \cite{Virgo} has rung in the age of GW astronomy. While all signals observed thus far have been of astrophysical origin, \textit{i.e.}, the coalescence of compact binaries \cite{GW_binary}, it is expected that GWs will also open a window on cosmology in the foreseeable future \cite{GW_cosmology}. Within the next decades, a multitude of GW observatories will go online, ranging from third-generation ground-based interferometers over satellite-borne interferometers in space to pulsar timing arrays monitored by new radio telescopes (see \cite{GW_survey} for an outlook on GW astronomy in the 2020’s). These experiments promise to be sensitive to a wealth of hypothetical cosmological GW signals — such as the stochastic GW background (SGWB) from inflation, GWs from phase transitions in the early Universe, or GWs emitted by topological defects (see \cite{GW_topological} for recent review articles) — and even to anisotropies in the GW signal \cite{GW_anisotropies}. The direct observation of any of these cosmological signals would allow one to chart unexplored territory that cannot be accessed by conventional cosmological probes such as the cosmic microwave background (CMB) or the primordial abundances of light elements generated during Big Bang nucleosynthesis (BBN).

In this paper, we will be concerned with the primordial SGWB from inflation \cite{GW_inflation} (see \cite{GW_inflation_review} for a review). An intriguing feature of inflationary GWs is that they act as a logbook of the expansion history of our Universe throughout its evolution \cite{GW_logbook}. Indeed, the detailed time evolution of the Hubble rate during the expansion determines the transfer function that describes how gravitational waves at different frequencies are redshifted to the present day. This property turns primordial GWs into a powerful tool that grants access to the thermal history of our Universe prior to BBN. Primordial GWs offer, \textit{e.g.}, an opportunity to measure the reheating temperature after inflation \cite{GW_reheating, GW_reheating_review, GW_reheating_recent}. Similarly, they may be used to infer the equation of state (EOS) during the quark-hadron phase transition in quantum chromodynamics \cite{GW_qcd, GW_qcd_recent} or constrain properties of hidden sectors beyond the Standard Model (BSM) \cite{GW_hidden, GW_hidden_recent}.

The same may also be true for GWs emitted by cosmic strings \cite{GW_cosmic_strings, GW_cosmic_strings_recent}, whose detailed properties are currently under discussion (see \cite{GW_cosmic_strings_review} and references therein).

The main goal of this paper is to demonstrate how future observations of the primordial SGWB from inflation across a large range of frequencies will be instrumental in constraining BSM physics. To this end, we shall consider a broad class of new physics models in which the presence of a scalar field \(\phi\) in the early Universe leads to a modified expansion history. Such a situation can occur in a variety of BSM scenarios. Possible BSM scalar fields that \(\phi\) may be identified as include, but are not limited to: the Polonyi field in models of gravity-mediated supersymmetry breaking \cite{GW_supersymmetry, GW_supersymmetry_recent}, a modulus field in four-dimensional compactifications of string theory \cite{GW_string, GW_string_recent}, a flavon field in extensions of the Standard Model (SM) that aim at explaining the flavor structure of quark and leptons (\textit{such as}, \textit{e.g.}, the Froggatt-Nielsen flavor model \cite{GW_flavor}), and the saxion field in supersymmetric axion models \cite{GW_axions, GW_axions_recent}.

At some point prior to BBN, the energy density stored in the coherent oscillations of the scalar field begins to dominate over radiation. The ensuing era of scalar-field domination (SD), or \textit{scalar era} for short, leads to a characteristic feature in the transfer function for primordial GWs, which may be detected by future GW experiments. In a detailed numerical analysis, we calculate the transfer function for primordial GWs that captures the modified expansion during the scalar era. This allows us to determine the final GW spectrum across the entire relevant parameter space of our scalar-field model. For each parameter point, we compute the signal-to-noise ratios (SNRs) at which the GW spectrum as well as individual features in this spectrum are expected to be observed by various future GW experiments. The outcome of our analysis is a global picture of the GW signature of the scalar era and the experimental prospects of detecting it. Our study highlights the complementarity of future GW experiments across the entire range of accessible frequencies and defines an important benchmark scenario for the experimental GW community in the coming decades.
Primordial gravitational waves. GWs correspond to spatial tensor perturbations \( h_{ij} \) of the spacetime metric,  
\[
 ds^2 = -dt^2 + a^2(t) \left[ \delta_{ij} + h_{ij}(t, \mathbf{x}) \right] dx^i dx^j ,
\]
where \( a \) denotes the cosmic scale factor and the symmetric tensor \( h_{ij} \) is evaluated in transverse-traceless gauge, \( h_{ii} = \partial_i h_{ij} = 0 \). The free propagation of GWs is governed by the linearized Einstein equation with a vanishing source term. In Fourier space, one thus obtains the following equations of motion for the tensor modes \( h_p^0 \),  
\[
 \frac{d^2}{dt^2} + \frac{2}{a(u)} \frac{da(u) \cdot d}{du} + 1 \right) h_p^0(u) = 0 .
\]
Here, \( k \) denotes the comoving 3-momentum with absolute value \( k = ||\mathbf{k}|| \), \( p = +, \times \) distinguishes the two possible polarization states of a GW, and the variable \( u = k \tau \) (with \( \tau \) denoting conformal time, \( dt = a d\tau \)) is a measure for the spatial extent of a GW. For \( u \ll 1 \) (\( u \gg 1 \)), a mode is located far outside (inside) the Hubble horizon.

An important property of inflationary GWs is that they are stretched to super-horizon size during inflation. For modes deep inside the horizon, one obtains the following GW spectrum at the present time,  
\[
 \Omega_{GW}^0(f) \simeq \frac{1}{12} \frac{k^2}{a_0^2 H_0^2} T_t(k) |\chi_k|^2 , \quad f = \frac{k}{2\pi a_0} ,
\]
where \( a_0 \) and \( H_0 = 100 h \text{ km/s/Mpc} \) represent the present values of the scale factor and the Hubble rate, respectively. The primordial tensor spectrum \( T_t \) depends on the initial conditions set by the inflationary period and is conventionally parametrized by a simple power law around the CMB pivot scale, \( k_{\text{CMB}} = 0.05 \text{ Mpc}^{-1} \),  
\[
 T_t = \frac{k^3}{\pi^2} \left( |\tilde{h}_k^+|^2 + |\tilde{h}_k^x|^2 \right) = A_t \left( \frac{k}{k_{\text{CMB}}} \right)^n_t .
\]
In this paper, we are interested in assessing the maximal reach of future GW experiments. For this reason, we decide to fix the primordial tensor amplitude at the maximally allowed value, \( A_t \approx 1.5 \times 10^{-10} \), that is consistent with the most recent upper bound on the tensor-to-scalar ratio, \( r = A_s / A_t \lesssim 0.07 \) \([55]\), where \( A_s \approx 2.1 \times 10^{-9} \) is the measured amplitude of the primordial spectral index is phenomenologically still completely viable. \( n_t = 0.4 \) complies with (1) the CMB constraints derived by the PLANCK Collaboration \([55]\), (2) the upper bound on the amplitude of an isotropic SGWB at \( O(10) \text{ Hz} \) frequencies by LIGO and Virgo \([62, 63]\), and (3) global bounds on primordial GWs (based, e.g., on BBN) across the full frequency spectrum \([64, 65]\).

The scalar era. We consider the dynamics of a real scalar field \( \phi \), employing an effective description in terms of three parameters: mass \( m_\phi \), decay rate \( \Gamma_\phi \), and initial field value \( \phi_{\text{ini}} \) at the end of inflation. We assume a harmonic potential around the origin in field space and some (direct or indirect) coupling to the Standard Model that allows \( \phi \) to decay to radiation at the end of its lifetime. The dynamical evolution of the field \( \phi \) is governed by the Klein-Gordon equation in an expanding background,  
\[
 \frac{d^2}{dt^2} + \left( 3 H(t) + \Gamma_\phi \right) \frac{d}{dt} + m_\phi^2 \right) \phi(t) = 0 ,
\]
where we included a friction term proportional to \( \Gamma_\phi \). The Hubble rate \( H \) follows from the Friedmann equation,  
\[
 H^2(t) = \frac{\left( \dot{a}(t) / a(t) \right)^2}{\rho_5} = \frac{\rho_5(t) + \rho_R(t)}{3 M_{Pl}^2} ,
\]
where \( M_{Pl} \approx 2.44 \times 10^{18} \text{ GeV} \) is the reduced Planck mass and \( \rho_5 = 1/2 \dot{\phi}^2 + 1/2 m_\phi^2 \phi^2 \) denotes the energy density stored in the field \( \phi \). The energy density of radiation, \( \rho_R \), is described by an evolution equation that follows from covariant energy conservation in an expanding universe,  
\[
 \frac{d}{dt} + 4 \frac{g_{s,s} \left( \rho_R(t) \right)}{g_{s,s} \left( \rho_R(t) \right)} H(t) \right) \rho_R(t) = \Gamma_\phi \dot{\phi}^2(t) ,
\]
where \( g_{s,s} \) and \( g_{s,p} \) are the effective numbers of relativistic degrees of freedom that contribute to the entropy and energy densities of radiation, respectively. We will evaluate \( g_{s,s} \) and \( g_{s,p} \) using the numerical data tabulated in \([26]\).

Let us now discuss the system of equations (5) to (7). First, we observe that \( \phi \) only begins to roll—and eventually oscillate around the origin in field space—once the Hubble rate has dropped below the scalar mass, \( H \lesssim m_\phi \). At earlier times, the Hubble friction term in (5) keeps \( \phi \) more or less fixed at \( \phi_{\text{ini}} \). For a sufficiently high reheating temperature after inflation, the expansion is initially
The nonstandard EOS and the late-time entropy injection during the scalar era result in the dilution of subhorizon tensor modes. This effect is captured by the dilution factor $D = \left[ S(T \gg T_{SD}) / S(T \ll T_{RD}) \right]^{1/3}$, where $S$ denotes the comoving entropy density, $S = a^3 \rho$,

$$D = e^{c / 3} d \left( \frac{g_{s,v}^{RD}}{g_{s,v}^{SD}} \right)^{1/3} \left( \frac{g_{\rho}^{RD}}{g_{\rho}^{SD}} \right)^{1/4} \eta^{1/6}. \quad (10)$$

The factor $d \approx 0.80$, which needs to be determined numerically, accounts for entropy production at $T < T_{RD}$. The factor $\eta$ is defined as the ratio of the two values of the Hubble rate at $T = T_{RD}$ and $T = T_{SD}$, respectively,

$$\eta = \frac{H_{RD}}{H_{SD}} = \frac{18 \alpha_{SD}^3 \alpha_{RD} \Gamma_{\phi} \left( M_{Pl} \right)^4}{b^4 c m_{\phi} \phi_{ini}^2}. \quad (11)$$

The two temperatures $T_{SD}$ and $T_{RD}$ also single out two frequencies in the GW spectrum, $f_{SD}$ and $f_{RD}$, which correspond to the tensor modes that re-enter the horizon at these temperatures, respectively. For $f_{RD}$, we find

$$f_{RD} = f_0 \left( \frac{g_{s,v}^{RD}}{g_{s,v}^{SD}} \right)^{1/3} \left( \frac{g_{\rho}^{RD}}{g_{\rho}^{SD}} \right)^{1/2} \left( \frac{\Omega_{R}^{0}}{1/2} \right)^{1/2} \frac{T_{RD}}{T_0}, \quad (12)$$

where $T_0 \approx 2.72548 \times 10^{10} \text{K}$ is the current temperature of the CMB [66], and $\Omega_{R}^{0} \approx 4.2 \times 10^{-5}$ denotes the energy density parameter of radiation at the present time, and $f_0 = H_0 / (2 \pi)$ corresponds to the frequency of the GW mode that currently stretches across one Hubble radius, $f_0 / h \approx 5.2 \times 10^{-5} \text{Hz}$. The frequency $f_{SD}$ can be computed in terms of the quantities in (11) and (12),

$$f_{SD} = \left( \frac{e^c}{\eta} \right)^{1/3} f_{RD}. \quad (13)$$

This shows that the parameter $\eta$ determines the duration of the scalar era in frequency space. In our numerical analysis, we will scan over different values of $\eta$ by varying the ratio $m_{\phi} / T_{\phi}$, while keeping the initial field value fixed at $\phi_{ini} = 10^{18} \text{GeV}$. This benchmark represents a typical value that can be realized in many models as an initial condition after inflation [67–70]. Aside from that, it is important to note that, to first approximation, it is straightforward to generalize our analysis to different values of $\phi_{ini}$ by simply rescaling all values of $m_{\phi} / T_{\phi}$.

**Transfer function.** For a mode with wave number $k$ deep inside the horizon, the transfer function roughly scales like $\chi_k \sim a_k / a_0$, where $a_k$ is the scale factor at the time of horizon re-entry, implicitly defined by $a_k = k / H(a_k)$ [20, 71, 72]. For an EOS $w = p / \rho = \text{const}$ (with pressure $p$ and energy density $\rho$), this results in a simple power-law scaling of the final GW spectrum,

$$\Omega_{GW}^{0} (f) \propto f^n, \quad n = n_t + \frac{2 (3 w - 1)}{3 w + 1}, \quad (14)$$

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which illustrates the main impact of the scalar era on the GW spectrum: For frequencies \( f_{\text{RD}} \lesssim f \lesssim f_{\text{SD}} \), the spectral index \( n \) changes by \( \Delta n \approx -2 \) compared to the spectrum at smaller and larger frequencies. This results in a step-like feature in the GW spectrum with two kinks located at \( f \approx f_{\text{RD}} \) and \( f \approx f_{\text{SD}} \), respectively (see Fig. 2). The ratio of the spectral amplitudes at these two frequencies is controlled by the dilution factor \( D \). Neglecting any changes in \( g_{s,\rho} \) and \( g_{s,s} \), we approximately find

\[
\frac{\Omega_{\text{GW}}^0(f_{\text{SD}})}{\Omega_{\text{GW}}^0(f_{\text{RD}})} \approx \left( \frac{f_{\text{SD}}}{f_{\text{RD}}} \right)^n D^4.
\]

(15)

To obtain a precise and accurate result for the transfer function, we numerically solve the coupled set of equations (2), (5), (6), and (7) for any choice of \( m_\phi \) and \( \Gamma_\phi \). Together with (3) and (4), this allows us to compute the final GW spectrum across our entire parameter space.

**Signal-to-noise ratios.** A GW experiment with strain noise power spectrum \( S_{\text{noise}} = 6 f_\nu^2 f_d^4 \Omega_{\text{noise}} \) is able to detect a stochastic signal \( \Omega_{\text{signal}} \) at the following SNR \([73,\]

\[
\text{SNR}^2 = N t_{\text{obs}} \int_{f_{\text{min}}}^{f_{\text{max}}} df \left[ \frac{\Omega_{\text{signal}}(f)}{\Omega_{\text{noise}}(f)} \right]^2,
\]

(16)

where \( t_{\text{obs}} \) denotes the experiment’s observing time and \( N = 1 \) (\( N = 2 \)) for experiments that perform an auto (cross) correlation measurement of the SGWB. With the full GW spectrum at hand, we are now able to forecast the SNRs for future ground-based interferometers [(1) the four-detector network (HLVK) consisting of advanced LIGO in Hanford and Livingston [2,3], advanced Virgo [4], and KAGRA [74,75], (2) Cosmic Explorer (CE) [76], and (3) Einstein Telescope (ET) [77–79]], future spaced-based interferometers [(1) LISA [80], (2) DECIGO [81,82], and (3) BBO [83–85]], and future pulsar timing arrays [(1) IPTA [86–88] and (2) SKA [89–91]]. We assume an observing time \( t_{\text{obs}} = 4 \) yr for all interferometer experiments and the equivalent [92] of \( t_{\text{obs}} = 20 \) yr for IPTA and SKA. In future work, one might consider refining our analysis by means of a Fisher information analysis. We, however, expect that such an analysis would only marginally improve over our SNR-based approach (see [37], which finds no difference between both approaches in the specific case of LISA).

In principle, it is also necessary to account for confusion noise from astrophysical sources (see, e.g., [93]). The significance of confusion noise, however, decreases over time, as larger observing times allow one to resolve and subtract a larger number of individual foreground sources. In what follows, we will therefore consider an idealized scenario without any foreground contamination. In this sense, our SNR forecasts may also be regarded as upper limits on what will be realistically achievable.

For each experiment, we compute two kinds of SNRs (see Fig. 3): First, we compute the total SNR based on the full GW signal, \( \Omega_{\text{signal}} \rightarrow \Omega_{\text{GW}}^0 \). If this SNR is larger than 1, we conclude that the respective experiment will have “at least a slight chance” of detecting a signal. Then, we compute a second, reduced SNR based on a subtracted GW signal, \( \Omega_{\text{signal}} \rightarrow \Omega_{\text{GW}}^0 - \Omega_{\text{fit}}^0 \), where \( \Omega_{\text{fit}}^0 \) represents a power-law fit of the GW spectrum around the frequency at which a given experiment is most sensitive. This construction is in accord with the matched-filter approaches in [37,94]. If the reduced SNR is larger than 100, we conclude that the respective experiment is “very likely” to detect a feature in the SGWB, i.e., a deviation from a pure power law, related to the scalar era. In practice, this feature will correspond to one or both of the two kinks at \( f \approx f_{\text{RD}} \) and \( f \approx f_{\text{SD}} \). Our choice of SNR threshold values allows us to assign the labels “at least a slight chance” and “very likely” to the different regions in Fig. 3 in a conservative manner. Meanwhile, we stress that our quantitative conclusions are nearly insensitive to \( \mathcal{O}(1) \) changes of these threshold values. Our qualitative conclusions are not affected at all by the precise values of the SNR thresholds.

**Discussion.** Our results in Fig. 3 are a powerful testament to the complementarity of future GW experiments. Consider, e.g., a scalar field with \( m_\phi = 10 \) GeV, \( \Gamma_\phi = 10^4 \) eV, and \( \phi_{\text{ini}} = 10^{18} \) GeV (point \( \circ \) in Fig. 3). In this case, the scalar era occurs at temperatures \( 5.4 \times 10^4 \lesssim T/\text{GeV} \lesssim 1.7 \times 10^6 \), which leads to a dilution factor \( D \approx 7.9 \times 10^{-2} \) and a modification of the GW spectrum at frequencies \( 1.6 \times 10^{-3} \lesssim f/\text{Hz} \lesssim 4.9 \times 10^{-1} \). This scenario can be directly probed by LISA, DECIGO, and BBO, all of which will observe a departure from a pure power law. At the same time, CE, IPTA, and SKA will detect the SGWB from inflation, while HLVK and ET will fail to observe a primordial signal. On top of
that, future CMB observations may confirm the blue tilt of the tensor spectrum. Along these lines, it is possible to translate every point in Fig. 3 into a list of predictions, i.e., a characteristic experimental fingerprint, for the GW experiments that we have considered in this paper.

The results of our analysis are applicable to a wide range of particle physics models that lead to a scalar era in the early Universe. In addition, it is important to note that the modified expansion history and late-time entropy production during the scalar era not only affect the spectrum of primordial GWs, but also the evolution of other cosmological relics, such as dark matter [96–103] and the baryon asymmetry of the Universe [104]. Finding evidence for a scalar era in future GW experiments would therefore have a profound impact on our understanding of BSM physics and early-Universe cosmology alike.

The analysis presented in this paper should only be regarded as a first step. Next, it will be necessary to relax our assumptions regarding the primordial tensor spectrum, the initial field value, and the shape of the scalar potential. Aside from that, it would be interesting to identify a self-consistent embedding of our scenario in a concrete inflationary model that is capable of generating a strongly blue-tilted tensor spectrum. We leave these steps for future work, concluding with the observation that a scalar era in the early Universe represents a fascinating possibility that awaits further exploration.

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FIG. 3: Experimental prospects to observe a signal or a even a feature in the GW spectrum (see text for details) in dependence of the model parameters $m_\phi$ and $\Gamma_\phi$. The three points ①, ②, ③ mark the parameter examples used in Figs. 1 and 2. The meshes drawn in the feature regions indicate where the frequencies $f_{BD}$ (meshes extending up to arbitrarily large $m_\phi$) and $f_{SD}$ (meshes extending up to a finite $m_\phi$) fall into the frequency ranges of the individual experiments (see Fig. 2).

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