Analysis of wind speed characteristics using different distribution models in Medan City, Indonesia

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ABSTRACT

Estimating wind speed characteristics plays an essential role in designing a wind power plant at a selected location. In this study, the Weibull, gamma, and exponential distribution models were proposed to estimate and analyze the wind speed parameters and distribution functions. Real measured data were collected from Medan City, Indonesia. The scale and shape factors of wind distribution for three years data were calculated. The observed cumulative probability of the three models was compared to predicted wind characteristics. The probability density function (PDF) and the cumulative density function (CDF) of wind speed were also analyzed. The results showed that the Weibull model was the best model to determine PDF, while the exponential model was the best model to determine CDF for the Medan City wind site.

Keywords:
Cumulative probability
Exponential distribution
Gamma distribution
Weibull
Wind energy

INTRODUCTION

Wind energy is one of the cheapest renewable energy, and it is a very large source of energy around the world. The global potential of wind energy is about 10 TW, and it can provide the world electricity needs as much as 35% [1]. According to IRENA reports [2], the world total installed capacity of wind energy is 622.70 GW in 2019. While Asia has reached 40% of the global installed capacity [3], Indonesia has a total installed capacity of 76 MW in 2019, and this value is only 0.03% of the total installed capacity in Asia.

Estimating wind speed characteristics is very important to assess the potential of wind energy [4], evaluate the performance of wind energy systems [5], and design a power plant at a selected location. Moreover, wind energy potential varies directly to the wind speed, and the small changes in wind speed will affect the amount of energy produced by the wind power plant. For these purposes, an appropriate wind model is required to accurately analyze the wind data measured at the site [6] because the wind energy is much related to the site and geographic conditions [7]. Another method to extrapolate wind data precisely is by using a site-specific wind power law [8].

The distribution function is one of the most widely used techniques, and it is vital for the analysis of performance losses in complex systems in engineering. In general, the distribution function can be used to predict and represent a variety of different phenomena. Moreover, it can also be applied to analyze the probability of wind speed. Characterizing the wind speed distribution function becomes simple when the measured histogram is correctly fitted with the analytical data [9]. The wind distribution function at certain
points can be interpreted as relative likelihood values. The wind distribution function also provides the frequency of wind speed [10], [11]. Wind distribution functions, such as the probability density function (PDF) and the cumulative density function (CDF) of the wind speed, are very crucial to determine the technical feasibility and the economic viability of a power plant project [12].

The popular distribution function to estimate wind energy is the Weibull distribution function. Weibull distribution function consists of shape and scale parameters, which can be calculated using several models available in the literature [13]-[15]. The shape factor identifies the width of the wind speed distribution and determines the peak wind distribution in any region [16]. The scale factor identifies the abscissa scale of wind distribution and the condition of most of the wind potentials in a particular location [17]. Mohammed et al. [18] applied the Weibull distribution function to analyze statistics on the maximum monthly wind speed and the minimum monthly wind speed in Zagora, Morocco. Mahmood et al. [19] also analyzed wind characteristics for the Al-Salman site in Iraq using Weibull distribution.

In the wind energy application, a two-parameter Weibull is widely used and accepted to estimate wind energy potential. The two-parameter Weibull is represented in the form of a computable and flexible mathematical function [20]. Modeling wind speed with a two-parameter Weibull yielded significant values as reported in [21]-[24]. Teimourian et al. [25] applied a two-parameter Weibull to investigate other feasible wind sites in Iran. Sumair et al. [26] used a two-parameter Weibull with energy pattern factor method to estimate Weibull parameters and assess wind potential in South Punjab. Sumair et al. [27] also compared two-parameter Weibull, Rayleigh, and lognormal distributions to model the wind potential of the coastal belt of Pakistan. The two-parameter Weibull performed the most accurately, and the Rayleigh distribution was found to be the least.

Mert and C. Karakuş [28] used the two-parameter Weibull, mixed Weibull, generalized gamma, and Burr 4-parameter distribution to describe the wind speed profile. They reported that the mixed Weibull distribution had a better match compared to the two-parameter Weibull [29]. In addition, estimating wind performance and assessment of the wind energy potential in wind energy planning projects using the two-parameter Weibull was not suitable for large-scale wind energy generation [10]. Three-parameter generalized gamma distribution [30] and normal distribution [31] were found to more accurately describe the wind characteristics compared to the two-parameter Weibull at different locations. Kollu et al. [32] developed a wind speed model based on Rayleigh and Weibull distributions. However, Weibull empirical data showed low confidence in the results, which prompted researchers to suggest various alternative analytic distributions, such as Gaussian inverse [33], lognormal [34], normal square root [35], Weibull inverse [36], the principle of maximum entropy [37], and Weibull-gamma composite [38]. Arreyndip et al. [39] suggested the general extreme distribution to analyze wind energy variation and potential. In recent years several studies have been conducted to assess the potential for wind energy potential by using single and mixed distributions [35], [36].

It is obvious that no particular model fits all cases. For different wind locations, investigations should be carried out to obtain a suitable model for designing a wind power plant [40]. The Weibull distribution was the most used to determine the PDF of wind speed. The gamma and exponential distribution were often employed to determine the PDF of wind speed. However, there was still not enough information available about which model among the Weibull, gamma, and exponential distributions, is suitable to estimate PDF and CDF of the wind speed. This study aimed to propose and compare the three aforementioned models in estimating the best distribution functions of the wind speed characteristics in Medan City, Indonesia.

2. RESEARCH METHOD

In this study, the wind speed data was collected at Medan City (2°27'-2°47'N, 98°35'-98°44'E), Indonesia. The historical monthly wind speed data for 2017-2019 was used to estimate the wind distribution function. Figure 1 shows daily wind speed from January 2017 to December 2019. Medan City is located at 2.5-37.5 meters above sea level and has significant wind potential. Medan City has a tropical rainforest climate with dry and wet seasons that are not very distinct. Medan City has the driest months from February to April and experiences the wettest month in October [41]. The average wind speed in Medan City is around 3.16 m/s with a standard deviation of 0.30433 [42].

2.1. Wind distribution functions

Three distribution function models were proposed to evaluate wind speed in Medan City, namely the Weibull, gamma, and exponential distribution functions. Each distribution function has its own probability distribution function (PDF) and cumulative distribution function (CDF). The PDF is used to
determine the probability of a random variable falling within a specific range of values. In contrast, the CDF is used to determine the distribution of multivariate random variables.

Weibull distribution function has the PDF as follows:

\[ f(v) = \frac{k}{c} \left( \frac{v}{c} \right)^{k-1} e^{-\left(\frac{v}{c}\right)^k}, \quad k > 0, v > 0, c > 0 \]  

The corresponding CDF of the Weibull distribution function is defined by

\[ F(v) = 1 - \exp \left[-\left(\frac{v}{c}\right)^k\right], \quad k > 0, v > 0, c > 0 \]  

where \( c \) and \( k \) are the scale and shape factors, respectively, and \( v \) is the observed wind speed (m/s).

Like the Weibull distribution, the gamma distribution function also has two parameters, i.e., a scale factor \( c > 0 \) and a shape factor \( k > 0 \) to control the wind speed distribution. The gamma PDF and CDF at observed wind speed \( v \) are defined as follows:

\[ f(v) = \frac{1}{c \Gamma(k)} v^{k-1} \exp \left[-\frac{v}{c}\right], \quad k > 0, v > 0, c > 0 \]  

\[ F(v) = \int_0^v \frac{1}{c} \frac{1}{\Gamma(k)} v^{k-1} e^{-\frac{v}{c}} dv, \quad v > 0, a \in (0, \infty) \]  

where \( \Gamma(a) \) is the gamma function:

\[ \Gamma(k) = \int_0^\infty v^{k-1} e^{-v} dv, \quad v > 0 \]  

Different from the Weibull and gamma distributions, the exponential distribution function has only one parameter to control the wind speed distribution, i.e., a scale factor \( c > 0 \). The exponential PDF and CDF at observed wind speed \( v \) are described as follows:

\[ f(v) = \frac{1}{c} \exp \left[-\frac{v}{c}\right], \quad v > 0, c > 0 \]  

\[ F(v) = 1 - \exp \left[-\frac{v}{c}\right], \quad v > 0 \]  

In a statistical method, the maximum likelihood (ML) can be applied to estimate the parameters of a probability distribution by maximizing a likelihood function [43]. According to this method, the shape \( k \) and scale \( c \) parameters are calculated to the total data points \( N \), as follows [44], [45]:

Figure 1. Daily wind speed at Medan City for three years

![Graph showing daily wind speed at Medan City for three years.](image-url)
3. RESULTS AND DISCUSSION

In this section, three proposed models, i.e., Weibull, gamma, and exponential, are applied to analyze wind speed parameters (scale and shape). The estimated wind speed distribution parameters of each model for the three years (2017-2019) are presented in Table 1, Table 2, and Table 3. Additionally, the yearly wind speed distribution parameters for 2017, 2018, and 2019 are also shown in the last row of Table 1, Table 2, and Table 3, respectively.

Table 1. Estimated distribution parameters of wind speed for 2017

|          | Weibull distribution | Gamma distribution | Exponential distribution |
|----------|----------------------|--------------------|-------------------------|
|          | Scale (c) | Shape (k) | Scale (c) | Shape (k) | Scale (c) |
| January  | 4.489     | 4.897    | 3.794     | 16.871     | 0.225     |
| February | 5.343     | 4.667    | 3.593     | 17.560     | 0.205     |
| March    | 5.549     | 4.930    | 3.766     | 19.169     | 0.196     |
| April    | 5.049     | 5.729    | 5.280     | 24.674     | 0.214     |
| May      | 5.717     | 5.820    | 4.873     | 25.817     | 0.189     |
| June     | 5.834     | 4.783    | 3.820     | 20.391     | 0.187     |
| July     | 5.848     | 4.373    | 3.157     | 16.798     | 0.188     |
| August   | 5.848     | 5.056    | 4.194     | 21.324     | 0.197     |
| September| 5.536     | 4.306    | 3.131     | 14.993     | 0.209     |
| October  | 5.261     | 4.631    | 3.690     | 17.484     | 0.211     |
| November | 5.449     | 4.572    | 3.472     | 17.280     | 0.201     |
| December | 4.585     | 4.556    | 3.525     | 14.767     | 0.239     |
| Yearly   | 5.373     | 4.560    | 4.356     | 21.618     | 0.202     |

Table 2. Estimated distribution parameters of wind speed for 2018

|          | Weibull distribution | Gamma distribution | Exponential distribution |
|----------|----------------------|--------------------|-------------------------|
|          | Scale (c) | Shape (k) | Scale (c) | Shape (k) | Scale (c) |
| January  | 4.849     | 4.897    | 3.794     | 16.871     | 0.225     |
| February | 5.318     | 4.744    | 3.687     | 17.952     | 0.205     |
| March    | 5.573     | 4.959    | 3.835     | 19.601     | 0.196     |
| April    | 5.029     | 5.722    | 5.296     | 24.638     | 0.215     |
| May      | 5.757     | 5.857    | 4.985     | 26.601     | 0.187     |
| June     | 5.857     | 4.747    | 3.772     | 20.201     | 0.187     |
| July     | 5.867     | 4.341    | 3.099     | 16.557     | 0.187     |
| August   | 5.456     | 5.187    | 4.457     | 22.365     | 0.199     |
| September| 5.354     | 4.161    | 2.905     | 14.128     | 0.206     |
| October  | 5.097     | 4.834    | 4.146     | 19.356     | 0.214     |
| November | 5.490     | 4.540    | 3.455     | 17.312     | 0.200     |
| December | 4.611     | 4.459    | 3.348     | 14.084     | 0.238     |
| Yearly   | 5.347     | 4.916    | 3.556     | 17.448     | 0.204     |

Table 3. Estimated distribution parameters of wind speed for 2019

|          | Weibull distribution | Gamma distribution | Exponential distribution |
|----------|----------------------|--------------------|-------------------------|
|          | Scale (c) | Shape (k) | Scale (c) | Shape (k) | Scale (c) |
| January  | 5.017     | 4.887    | 3.929     | 18.076     | 0.217     |
| February | 5.389     | 4.053    | 2.805     | 13.702     | 0.205     |
| March    | 5.053     | 3.833    | 2.488     | 11.347     | 0.219     |
| April    | 5.228     | 5.303    | 4.395     | 21.146     | 0.208     |
| May      | 5.303     | 4.813    | 3.608     | 17.540     | 0.206     |
| June     | 5.866     | 5.122    | 3.867     | 20.862     | 0.185     |
| July     | 5.095     | 6.952    | 7.447     | 35.495     | 0.210     |
| August   | 5.740     | 5.253    | 4.289     | 22.629     | 0.190     |
| September| 5.702     | 6.714    | 6.532     | 34.787     | 0.188     |
| October  | 5.833     | 5.725    | 4.662     | 25.170     | 0.185     |
| November | 5.596     | 5.688    | 4.833     | 25.036     | 0.193     |
| December | 6.113     | 6.048    | 5.093     | 28.906     | 0.176     |
| Yearly   | 5.496     | 5.266    | 3.902     | 19.752     | 0.198     |
The monthly wind parameters of the three proposed models are also compared (as seen in Figure 2, Figure 3, and Figure 4). The parameters for 2019 are very different from other years, and this is due to climate change which changes the wind speed. Changes in wind speed are not followed by changes in wind parameters properly. Changes in wind speed parameters can result in changes in the wind distribution functions. As shown in Figure 2, Figure 3, and Figure 4, changes in parameters occur in March, May, July, and the following months, wherein these months have a significant difference in temperature in 2019 compared to the other years.

Furthermore, comparisons of the performances of three distribution models for 2017, 2018, and 2019 by using the estimated parameters are shown in Figure 5, Figure 6, and Figure 7. The difference between the three models is very significant, especially in the exponential distribution model. This is due to the exponential distribution model only takes into account the scale factor, while the Weibull and gamma distributions use both scale and shape factors.

Figure 2. Estimated parameters of the Weibull distribution for three years

Figure 3. Estimated parameters of the gamma distribution for three years

Figure 4. Estimated parameters of the exponential distribution for three years
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The observed and expected cumulative probability for the three models in 2017, 2018, and 2019 are presented in Figure 8, Figure 9, and Figure 10, respectively. The expected cumulative probability of wind characteristics is a straight line and it is used as a data benchmark. Further investigations found that the exponential model is not around a straight line. This occurs because of the fluctuations in wind speed data due to climate change.

From scale and shape factors and distribution probability results, the PDF and CDF of wind speed characteristics for Medan City are analyzed. For wind speed characteristic in 2017 (as seen in Figure 11), it is found that Weibull distribution PDF and CDF are 0.365 and 58%, respectively, with the wind speed of 5.2 m/s. Gamma distribution gives PDF of 0.009 and CDF of 0.02%, with the wind speed of 7.2 m/s, while exponential distribution PDF and CDF are 0.045 and 74%, respectively, with the wind speed of 7.2 m/s.

For wind speed characteristic in 2018 (as seen in Figure 12), the Weibull distribution PDF and CDF are 0.348 and 57%, respectively, with the wind speed of 5.2 m/s, while the gamma distribution gives PDF of 0.000007 and CDF of 4%, with the wind speed of 7.2 m/s. In this case, the exponential distribution PDF and CDF are 0.046 and 77.5%, respectively, with the wind speed of 7.2 m/s.

For wind speed characteristic in 2019 (as seen in Figure 13), the PDF and CDF obtained by the Weibull distribution model are 0.345 and 51%, respectively, with a wind speed of 5.2 m/s. In the same case, the gamma distribution gives PDF of 0.09 and CDF of 3%, with the wind speed of 7.2 m/s, while the exponential distribution gives PDF and CDF of 0.048 and 73.0%, respectively, with the wind speed of 7.2 m/s.

In addition, the PDF and CDF of the Weibull, gamma, and exponential distribution models are tabulated as in Table 4. Table 4 shows that the Weibull distribution is the best model to determine PDF, followed by the exponential and gamma distributions. On the other hand, the exponential distribution is the best model to determine CDF, followed by the Weibull and gamma distributions.
Figure 8. Observed and expected cumulative probability for the three models in 2017

Figure 9. Observed and expected cumulative probability for the three models in 2018

Figure 10. Observed and expected cumulative probability for the three models in 2019

Table 4. Comparison PDF and CDF for three models

|          | Weibull model | Gamma model | Exponential model |
|----------|---------------|-------------|------------------|
|          | PDF           | CDF (%)     | PDF              | CDF (%)     | PDF            | CDF (%)     |
| 2017     | 0.365         | 58.0        | 0.009            | 0.02        | 0.045          | 74.0        |
| 2018     | 0.348         | 57.0        | 0.000007         | 4.00        | 0.046          | 77.5        |
| 2019     | 0.345         | 51.0        | 0.09             | 3.00        | 0.048          | 73.0        |
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Figure 11. PDF and CDF: (a) Weibull, (b) gamma, (c) exponential distribution models for 2017
Figure 12. PDF and CDF: (a) Weibull, (b) gamma, (c) exponential distribution models for 2018
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4. CONCLUSION

Three different models have been applied to estimate parameters and distribution functions of wind speed in Medan City. Comparisons of the performances of three distribution models for 2017, 2018, and 2019 wind data showed that the exponential model performed very differently from the Weibull and gamma models. The observed cumulative probability of wind characteristics by using the exponential model did not fit the expected values. However, the exponential distribution was found as the best model to determine CDF, followed by the Weibull and gamma distributions. On the other hand, the Weibull distribution was the best model to determine PDF. The gamma model gave the worst performances in determining both CDF and PDF values.

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