Nano-twinning in a $\gamma'$ precipitate strengthened Ni-based superalloy

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ABSTRACT
Twinning has been found to be a dominate mechanism in the $\gamma'$ precipitate strengthened Ni-based superalloys during service at intermediate temperatures. Here, high-resolution transmission electron microscopy and atomistic simulations have been combined to show that the twin nucleation process can be facilitated by Co replacing a fraction of Al in the $\gamma'$ precipitates, due to the negative binding energy of Co–Co atoms. The study further reveals that the presence of Co promotes a new twinning pathway featured with nucleation of one complex stacking fault (CSF) on the middle plane in between two separated CSFs.

IMPACT STATEMENT
We demonstrate that Co in the $\gamma'$ precipitates promotes a new twinning pathway featured with nucleation of one CSF on the middle plane between two separated CSFs.

Twinning is generally considered as a mechanism contributing to the strength and plasticity of metallic materials, and will be facilitated under low temperatures and/or high strain-rate conditions [1,2]. Nonetheless, there exists an exception for Ni-based superalloys, which typically have $\sim 50\%$ volume fraction of ordered L1$_2$ structured $\gamma'$ (Ni$_3$Al type) precipitates coherently embeded in the disordered face-centered cubic (fcc) $\gamma$ matrix [3–7]. Deformation twinning was identified as a dominant mechanism in Ni-based superalloys during low strain rate creep and tension at a wide range of temperatures, 650–760$^\circ$C [8–10], which imparts the nano-twins on the order of several to tens of atomic layers. The properties at elevated temperatures are believed to arise from the resistance of $\gamma'$ precipitates to the shear of Shockley partial dislocations and the subsequent rate-limiting process for twinning on the adjacent $\{111\}$ planes in the $\gamma'$ precipitates [4–10]. Based on the limited high-resolution transmission electron microscope (HRTEM) studies on the evolution of twins in Ni-based superalloys [6,8], it has been proposed that twin nucleation may be accomplished by successive $1/6 < 112 >$ Shockley partial dislocations on contiguous $\{111\}$ planes. Unlike the scenario in the disordered fcc structure, gliding of $1/6 < 112 >$ twinning partials in the Ni$_3$Al-$\gamma'$ precipitates will create high energy Al–Al nearest neighbor violations at the stacking fault (SF), resulting in the formation of a complex stacking fault (CSF) [6,8,9,11]. The formation of high energy Al–Al violations suggests that the tendency for the $\gamma'$ precipitates to accommodate deformation by twinning is very low [1,12]. Obviously, this is at odds with the TEM observations of numerous nano-twins in the $\gamma'$ precipitates strengthened Ni-based superalloys [4–10,13].

In the present work, HRTEM observations and atomistic simulations are combined to demonstrate that the twin nucleation process can be facilitated by replacing a fraction of the Al atoms with Co in the Ni$_3$Al-$\gamma'$

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precipitates, which significantly reduces the chance for the formation of Al–Al bonds. Furthermore, HRTEM observations on an embryo of a three-layer twin provide the evidence of a new twinning pathway in the $\gamma'$ precipitates, which is featured with nucleation of one CSF on the middle plane between two separated CSFs. This new twinning route has a lower energy barrier as compared to the classical twinning model with successive twinning partials gliding on consecutive $\{111\}$ planes. Our results provide a new physical understanding on the twin nucleation process and the role of Co in the ordered L1$_2$ structured $\gamma'$ precipitates of Ni-based superalloys.

The current study was performed on a $\gamma'$ precipitate strengthened Nickel-based superalloy with Co, Cr, Al and Ti as the major alloying elements (see Table 1). The alloy samples were subjected to a solution anneal for 4 h at 1090°C followed by air cooling, and subsequent ageing for 24 h at 650°C and 16 h at 760°C. The resultant microstructure consists of a disordered $\gamma$ matrix with ordered L1$_2$ $\gamma'$ precipitates with a mean size of $\sim$ 50 nm. The alloy specimens with a gage section of $\phi$ 5 mm $\times$ 25 mm were tensioned to a uniform strain of $\sim$ 4% with a strain rate of $8 \times 10^{-5}$ s$^{-1}$ at 675°C. The TEM specimens were prepared by slicing foils from the gage along the tensile axis by wire electric discharge machining, and then mechanical grinding with SiC papers. The TEM foils were finally thinned down to electron transparency in a Struers Tenupol 5 twin jet polishing unit using an electrolyte consisting of 85% ethanol and 15% perchloric acid at a temperature of $-20^\circ$C and a voltage of 20 V. HRTEM analyses were performed on a Titan G2 60-300 with an energy dispersive X-ray spectroscopy (EDS), and a Titan Cubed Themis G2 microscope operated at 300 keV. To rationalize the observed phenomenon related to the twinning at the atomic scale, we calculated the generalized stacking/planar fault energy (GSFE/GPFE) for different systems using EAM potentials [14,15] and the LAMMPS code [16].

After tension to 4% plastic strain at 675°C, the dominant substructures within grains were found to be the highly aligned, planar defects, which propagated through both the $\gamma$ matrix and $\gamma'$ phases. Figure 1(a) shows a bright field TEM image of the typical microstructure viewed along $[011]$ zone axis, i.e. a high density of faulted structures, and the inserted selected area diffraction (SAD) pattern displays the superposition of the reflections from $\gamma$ matrix, $\gamma'$ phases, and the $\{111\}$ twins, which unambiguously identifies twinning as a prevalent deformation mechanism. Close inspection of the twins in multiple grains by the HRTEM imaging reveals that nano-twinning in this $\gamma'$ strengthened Ni-based alloy imparts extremely thin nano-twins, which are usually on the order of 3–20 atomic layers. An example of an HRTEM micrograph of a five-layer-thick twin shearing the $\gamma'$ precipitate is shown in Figure 1(b).

**Table 1.** Nominal composition of the Ni-Co–Cr alloy in at.% together with compositions of $\gamma$ and $\gamma'$ determined by EDS in the HRTEM.

| Element | Nominal (at.%) | $\gamma'$ (at.%) | $\pm S_m$ | $\gamma$ (at.%) | $\pm S_m$ |
|---------|----------------|-----------------|------------|----------------|------------|
| Ni      | 48.70          | 66.65           | 5.24       | 44.12          | 1.83       |
| Co      | 22.94          | 11.76           | 2.00       | 30.17          | 2.24       |
| Cr      | 15.46          | 2.53            | 2.25       | 16.59          | 1.26       |
| Al      | 5.10           | 6.72            | 0.48       | 1.57           | 1.16       |
| Ti      | 4.96           | 8.29            | 1.18       | 1.94           | 1.50       |
| Mo      | 1.81           | 0.33            | 0.74       | 1.43           | 1.44       |
| W       | 0.34           | 0.80            | 1.18       | 1.82           | 1.84       |
| Fe      | 0.51           | 2.93            | 1.31       | 2.36           | 0.86       |
| Zr      | 0.02           | n.d.            | n.d.       | n.d.           | n.d.       |
| C       | 0.11           | n.d.            | n.d.       | n.d.           | n.d.       |
| B       | 0.06           | n.d.            | n.d.       | n.d.           | n.d.       |

![Figure 1](https://via.placeholder.com/150)

**Figure 1.** Typical microstructure of the deformed Ni-Co–Cr superalloy: (a) bright-field TEM image with inserted SAD, where $\gamma'$ and $T$ indicates the diffraction spots from $\gamma'$ precipitates and nano-twins, respectively; (b) HRTEM image of a five-layer twin with inserted Fourier transform.
It has been commonly believed that a nano-twin in the \( \gamma' \) strengthened Ni-based alloys can be nucleated through successive \( 1/6 <112> \) type of twinning partials gliding on consecutive planes \([6,8,12]\). In other words, a three-layer twin can be nucleated by adding one CSF immediately above or below two CSFs which serves as a nucleus \([17]\). Figure 2(a) shows an HRTEM image of two-layer CSFs on contiguous \( \{111\} \) planes. In the following analysis, BC in the Thompson tetrahedron is taken to be perpendicular to the page and the twin is formed by gliding of partial dislocations on the plane (a). Detailed analyses of the Burgers circuits \([18,19]\) revealed that \( b_1 \) and \( b'_1 \) are 90°, 30° \((\alpha D, C\alpha)\) dislocations dissociated from a perfect dislocation CD, while \( b_2 \) and \( b'_2 \) are 30°, 30° \((\alpha C, C\alpha)\) dislocations (Figure 2(b,c)). Consequently, a three-layer twin can be initiated on the two-layer CSFs in Figure 2(a) by adding one CSF bounded by 30°, 90° \((\alpha C, D\alpha)\) dislocations dissociated from a perfect dislocation DC \([10]\). However, it is important to note that a vast number of CSFs are also present in a pair on parallel \( \{111\} \) planes separated by one atomic layer rather than on neighboring planes, as shown in Figure 2(d). Unlike the two-layer CSFs, overlapping of two CSFs on parallel non-neighboring planes usually occurs only at the region where one SF gliding ahead another one, giving rise to a small overlapped area with four faulted layers, as marked by solid yellow lines in Figure 2(d). Further analysis on the Burgers circuits surrounding each end of two CSFs revealed that the CSFs are bounded by \( b_3, b'_3 \) of 30°, 90° \((\alpha C, D\alpha)\) dislocations dissociated from a perfect dislocation DC, and \( b_4, b'_4 \) of 30°, 30° \((\alpha C, C\alpha)\) dislocations (Figure 2(e–g)), confirming the fact that two CSFs on non-neighboring planes are also formed by the motion of \( 1/6 <112> \) type dislocations on parallel planes separated by one middle layer. Close inspections of more than 20 CSFs in a pair revealed that two CSFs lying on non-neighboring planes separated by one middle atomic layer constitutes 48%, indicating a high probability of Shockley dislocations gliding on non-neighboring planes in the \( \gamma' \) strengthened nickel alloys loaded at intermediate temperatures.

Figure 3(a) shows an example of the HRTEM image of an embryo of a three-layer twin with four atoms in length due to the approaching of three CSFs, as indicated by the yellow arrow. Analyses of Burgers circuits and atomic stacking sequences associated with the three-layer twin embryo revealed that the Burgers vectors of Shockley dislocations on the left end, i.e. \( b_1, b_2 \) and \( b_3 \), are all 30° \((\alpha C)\) Shockley partials (see Figure 3(b)). The Mahajan–Chin model suggested that two 30° \((\alpha C, C\alpha)\) and one 90° \((\alpha C)\) Shockley partials were assigned to an end of a three-layer twin where the twin initiated to maintain zero net displacement at the interface \([17]\). The very limited HRTEM observations conducted on the dislocation configurations of the three-layer twins are also consistent with the Mahajan–Chin model \([10,17]\). Thus, it is unlikely that the three-layer twin embryo shown in Figure 3(a) was formed as a result of one CSF moving to the two layer CSFs on the right, given the identical dislocation assignation to the left end. A new plausible
scenario for the twin nucleation we can envision is one
CSF nucleated on the middle plane between CSF I and
CSF III on parallel non-neighboring planes, and then
followed with approaching the overlapped area of the
two separated CSFs from right to left to form the twin
embryo. By comparing the dislocation configurations
at the ends of the twin embryo in Figure 3(a) with those
of the observed two separated CSFs, it is conceivable to
visualize the conversion of the two separated CSFs into
a three-layer twin embryo as follows. Consider a situa-
tion of Figure 3(a) as CSF III is bounded by a 90° (Da)
Shockley partial on the right end which are not captured
by HRTEM imaging, and consequently the dislocation
configurations of CSF I and CSF III comply with those of
two separated CSFs in Figure 2(d), i.e. $b_1$, $b'_1$ are 30° ($\alpha C$, $C_a$) Shockley dislocations, while $b_2$, $b'_2$ are 30°, 90° ($\alpha C$, $D_a$) Shockley partials, respectively (see Figure 3(b)).
Due to the fact that the Burgers vector of the left disloca-
tion with CSF II ($b_2$) is 30° ($\alpha C$) Shockley partial, it is
envisioned that the twin embryo in Figure 3(a) is formed by
nucleating a CSF II bounded by 30°, 30° ($\alpha C$, $B_a$) Shockley partials, which are dissociated from a perfect
dislocation BC on the middle plane between CSF I and
CSF III, as illustrated in Figure 3(b). Consequently, the
total Burgers vector of the dislocations constituting the
right end is equal to zero such that the three Shockley
partials on the left could glide away from the junction
and expand the twinned region (see Figure 3(b)). It is
interesting to note that the nature of the Shockley par-
tials constituting the ends of the three-layer twin formed
via this proposed twinning route (Figure 3(b)) is same as
those of Mahajan–Chin model [1,17,20].

The lattice resistance of different processes involved
in twin formation can be evaluated by the concept of
GSFE/GPFE [21,22], as shown in Figure 4. The simula-
tion cell had dimensions of $15 \times 15 \times 15$ nm in the [110],
[112] and [111] crystallography orientations of the fcc
lattice, respectively, and periodic boundary conditions
were imposed in both the [110] and [112] directions. The
upper half was shifted relative to the lower half along the
(111) plane in the [112] direction, followed by energy
minimization using the EAM potentials [14,15], to cal-
culate the GSFE/GPFE. Relaxations in [110] and [111]
directions were all allowed. In the $\gamma$ phase Ni, after
the first fault is formed (denoted as route ‘1’), the formation
of the second and third planar fault (denoted as ‘1-2’ and
‘1-2-3’, respectively) on successive planes are found to be
easier (see Figure 4(a)). Alternatively, when the forma-
tion of the second planar fault is skipped and an SF is
formed on a plane one layer above an existed SF (denoted
as ‘1-3’), the energy required is found to be higher than
that for the ‘1-2’ and ‘1-2-3’ processes, indicating that for-
tomation of planar faults on successive planes is energeti-
cally more favorable. Nonetheless, if two SFs separated by
one atomic layer are already formed, presumably as inde-
pendent nucleation events, and eventually meet/overlap
as they expand, the subsequent formation of a planar
fault in between them (denoted as ‘1-3-2’) that leads to
a twin nucleation is found to be much easier. Thus two
different pathways for the nucleation of a twin embryo
could be both operating. This is consistent with obser-
vations of nano-twins in the nanocrystalline Ni where
copious grain boundaries serve as the sources for twin-
ning partials [23]. Moreover, the twinning route 1-3-2
were observed in the nanocrystalline fcc Pt [24] and also
Cu [25]. In the Ni$_3$Al-$\gamma'$ phase, the opposite is found
be true (see Figure 4(b)). After the first CSF is formed,
formation of second and third planar fault on successive
planes and formation of a planar fault in between two
CSFs separated by one atomic layer are all found to be
more difficult; whereas formation of a CSF on a plane one
layer above an existed CSF is found to be slightly easier.
It is thus suggested that neither route 1-2 nor route 1-3 is
expected to be operating, and twinning is highly unfavor-
able in the $\gamma'$ phase, which is contrary to the experi-
mental observations of Ni-based superalloys [4–10,13].

It is noted that adding of Al increases the stable SF
energy of Ni from 134 to 210 mJ/m$^2$, and the energy
increase actually originates from the unfavorable Al–Al
bonds (also called forbidden bonds [3]) formed in
the faulted structure (see Figure 4(b,d)). The forma-
tion energy of a substitutional Al in fcc Ni is negative,
$0.87$ eV, indicating that Al–Ni bonds is highly preferred
in fcc Ni; whereas the formation energy of a pair of sub-
stitutional Al atoms in fcc Ni is $-1.45$ eV, indicating a
positive binding energy of Al–Al atoms, 0.29 eV. This is

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**Figure 3.** (a) HRTEM image of a three-layer-thick twin nucleated from two parallel CSFs on glide planes separated by one middle layer; (b) schematic of the dislocation configurations that constitute the three-layer twin in (a).
because the cohesive energy of fcc Al is $-3.36$ eV, much higher than that for fcc Ni, $-4.45$ eV. The positive binding energy of Al–Al atoms actually suggests that Al–Al bond is highly energetically un-preferred.

It is important to note that the actual atomic Al/Ni ratio (6.7 vs. 66.7 at.%) in the Ni$_3$Al-$\gamma'$ phase of the present alloy is not 1/3. The insufficiency of Al indicates that other alloying elements must occupy Al sites, presumably Co (11.8 at.%) and Ti (8.3 at.%). The calculation conducted on the Co (cohesive energy $-4.38$ eV for fcc Co) demonstrate that the formation energy of a substitutional Co in fcc Ni is also negative, $-0.20$ eV. On the contrary, the formation energy of a pair of substitutional Co atoms in fcc Ni is $-0.61$ eV, indicating a negative binding energy of Co–Co atoms, $-0.21$ eV. The preferred Co–Co bond actually reduces the energy of a twin structure. For example, if half of the Al atoms in Ni$_3$Al structure are randomly replaced by Co atoms to form Ni$_6$AlCo, the energies required for the twinning route of either 1-2-3 or 1-3-2 are significantly reduced, as shown in Figure 4(c–d). Therefore, both twinning mechanisms are expected to be operating again like in Ni. Furthermore, it is important to note that the twinning route 1-3-2 has a lower energy barrier as compared to the conventional route 1-2-3, which validate the experimental observations of the new twinning pathway. The replacement of Al with Co and the negative Co–Co binding energy thus explain the high tendency for twinning in the $\gamma'$ phase of Ni-based superalloys with high content of Co in the literature [5–7,9,10].

In conclusion, HRTEM observations combined with atomistic simulations serve to illustrate that enhanced twinning tendency in $\gamma'$ phase is induced by the high content of Co replacing a fraction of Al in the Ni$_3$Al-$\gamma'$ precipitates. The replacement of Al with Co significantly reduces the chance for the formation of high energy Al–Al bonds, and the negative binding energy of Co–Co atoms considerably lowers the energy barrier for twinning in the $\gamma'$ phase. Furthermore, a fault configuration featured with two CSFs separated by one middle layer is identified as a precursor to nano-twinning, which facilitates a new twinning pathway that has a much lower energy barrier as compared to the classical one. These results provide a physical insight to tailor the performance of Ni-based superalloys at elevated temperatures through alloying, which is essential to the design of
superalloys towards more critical aero-engine applications.

**Disclosure statement**

No potential conflict of interest was reported by the authors.

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