Soft Matter

PAPER

LCST polymers with UCST behavior†

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In this study, temperature dependent behavior of dense dispersions of core crosslinked flower-like micelles is investigated. Micelles were prepared by mixing aqueous solutions of two ABA block copolymers with PEG B-blocks and thermosensitive A-blocks containing PNIPAM and crosslinkable moieties. At a temperature above the lower critical solution temperature (LCST), self-assembly of the polymers resulted in the formation of flower-like micelles with a hydrophobic PEG shell and a hydrophilic core. The micellar core was stabilized by native chemical ligation (NCL). Above the LCST, micelles displayed a radius of \( \sim 55 \) nm, while a radius of \( \sim 48 \) nm was found below the LCST due to hydration of the PNIPAM core. Concentrated dispersions of these micelles \((\geq 7.5 \text{ wt})\) % showed glassy state behavior below a critical temperature \((T_c; 28 \, ^\circ\text{C})\) which is close to the LCST of the polymers. Below this \( T_c \), the increase in the micelle volume resulted in compression of micelles together above a certain concentration and formation of a glass. We quantified and compared micelle packing at different concentrations and temperatures. The storage moduli \((G')\) of the dispersions showed a universal dependence on the effective volume fraction, which increased substantially above a certain effective volume fraction of \( \varphi = 1.2 \). Furthermore, a disordered lattice model describing this behavior fitted the experimental data and revealed a critical volume fraction of \( \varphi_c = 1.31 \) close to the experimental value of \( \varphi = 1.2 \). The findings reported provide insights for the molecular design of novel thermosensitive PNIPAM nanoparticles with tunable structural and mechanical properties.

1. Introduction

Poly(N-isopropylacrylamide) (PNIPAM) is an attractive polymer for biomedical, biotechnological and pharmaceutical applications due to its thermo-responsive phase transition at a temperature close to body temperature.1–14 This polymer exhibits a lower critical solution temperature (LCST) in aqueous solution at 32 °C. Below this temperature, the polymeric chains are hydrated and therefore soluble in water, while upon increasing the temperature above the LCST, dehydration occurs and thus the polymer becomes insoluble.2 Amphiphilic di- or triblock (co)polymers of PNIPAM and polyethylene glycol (PEG) have been extensively studied for the preparation of thermosensitive polymer micelles as potential drug delivery vehicles.5–8 During the past years, there is a growing interest in strategies to convert PNIPAM based hydrogels into micelles for drug delivery applications.9–11 Unlike micelles, several studies have been devoted to the rheological characterization of dense dispersions of PNIPAM based microgels.12–15 PNIPAM (sub)micron gel particles are usually synthesized using free radical precipitation polymerization to yield small hydrogel particles \((\sim 0.2 \text{ to } 0.5 \, \mu\text{m} \text{ radius})\).16 These PNIPAM based microgels display thermosensitivity17 and a volume phase transition temperature (VPTT),18 which is close to the LCST of the polymer.19 This reversible transition temperature plays a crucial role in the viscoelastic behavior of dense dispersions of PNIPAM microgels. In general, when the temperature is below the VPTT, soft PNIPAM microgels are swollen resulting in high repulsive interparticle interactions caused by the steric hindrance of swollen polymer chains. At this temperature, the hydrated particles can be packed well above the random close packing fraction \( \varphi_{\text{rcp}} \approx 0.64 \).20,21 Due to compression and deformation of the particles, this leads to the formation of a glass exhibiting viscoelastic properties, which resembles pastes and colloidal glasses of hard spheres.22–24 At temperatures above the VPTT, dehydration of PNIPAM chains leads to shrinkage of the microgels and in this state, a raise in hydrophobic and van der Waals interactions due to high polymer density results in increased attractive interparticle
interactions. A variety of states depending on the magnitude of repulsive and attractive interactions have been reported for PNIPAM based microgel particles. A balance between attractive and repulsive interactions results in the formation of colloidal gels, whereas when the attractive forces exceed the repulsive interactions, macroscopic precipitation occurs. Dominancy and magnitude of repulsive or attractive interparticle interactions can be altered by introducing hydrophobic and/or hydrophilic monomers into PNIPAM based microgels. For instance, gelation properties of PNIPAM microgels have been tuned by changing surface charge density through copolymerization of PNIPAM with monomers such as acrylamide,25 fumaric acid,26 and acrylated hybrid oligomers composed of copolymers of NIPAM and fumaric acid behaved similarly as PNIPAM microgels without the comonomer and displayed colloidal gel behavior at $T > VPTT$. On the other hand, at a pH < $pK_a$, the surface of the particles is negatively charged due to deprotonation of the carboxylic groups, which in turn led to significant charge repulsion between the microgel particles. Consequently, due to the high repulsive forces at this pH, the microgels displayed liquid behavior at $T > VPTT$. Very recently, Es Sayed et al. reported on the synthesis of PNIPAM based microgel particles by surfactant-free precipitation copolymerization of PNIPAM and PEG-methacrylate. In the so-obtained microgel particles, PEG chains are present on their surface, however, this arrangement is not likely in a well-defined core–shell structure. They demonstrated that this microgel system has a higher colloidal stability than non-PEGylated ones. However, the effect of PEG on rheological characteristics of microgels was not described in this publication.

In contrast to microgels, PNIPAM based micelles are nanosized particles (10–100 nm diameter) formed by self-assembly of amphiphilic block copolymers of PNIPAM-PEG in aqueous solutions at concentrations above the critical micelle concentration (CMC) and above the LCST of the PNIPAM block. Therefore, PNIPAM based micelles with a PEG shell have a great potential as a well-defined core–shell structure particle for investigating the effect of PEG on rheological properties of dense PNIPAM based colloids.

In the present contribution, mechanical properties of concentrated dispersions of core crosslinked flower-like micelles having a PEG shell and a thermosensitive PNIPAM core were explored. Hydrodynamic radius of micelles was studied in their dilute dispersions at temperatures at temperatures below and below the LCST of the polymers using dynamic light scattering (DLS). Subsequently, the rheological properties (dynamical moduli in both linear and non-linear regime) of a series of concentrated micellar dispersions were studied over a temperature range of 10 to 40 °C. A theoretical model was used to describe the observed rheological behavior of the dispersions.

2. Materials and methods

2.1. Materials

All commercial chemicals were obtained from Sigma-Aldrich (ZWijndrecht, The Netherlands) and used as received unless indicated otherwise. $N\{-2$-hydroxypropyl]methacrylamide (HPMA) was synthesized by a reaction of methacryloyl chloride with 1-amino-prop-2-ol in dichloromethane according to a literature procedure. $N\{-2$-hydroxypropyl]methacrylamide-Boc-$S\-acacetimidomethyl-$L$-cysteine (HPMA-Boc-Cys(Acm)) and $N\{-2$-hydroxypropyl]methacrylamide-ethyliodiglycolate succinic acid (HPMA-ETSA) were synthesized according to previously reported procedures. Viscous Blue 420 Maleimide was obtained from Ursa BioScience (Maryland, USA). Phosphate buffered saline 10× (PBS) pH 7.4 (1.37 M NaCl, 0.027 M KCl and 0.119 M phosphates) BioReagents was purchased from B. Braun (Melsungen, Germany). Poly(ethylene glycol) bis(2-bromoisobutyrate) with a molecular weight of 6 kDa was synthesized by a method previously reported. Dialysis tubes (molecular weight cutoff (MWCO) 10 kDa) were obtained from Fisher Scientific (Bleiswijk, The Netherlands). PD-10 desalting columns were purchased from GE Healthcare (Uppsala, Sweden). PEG standards (molecular weights ranging from 106 to 969 000 Da) for GPC characterization were purchased from Agilent Technologies BV (Santa Clara, US).

2.2. Polymer synthesis and characterization

2.2.1. Synthesis of P(NIPAM-co-HPMA-Cys)-PEG-P(NIPAM-co-HPMA-Cys), PNC and P(NIPAM-co-HPMA-ETSA)-PEG-P(NIPAM-co-HPMA-ETSA), PNE. PNC and PNE were synthesized by atom transfer radical polymerization (ATRP) in solvent mixtures of 2.8 mL water and 0.9 mL of acetonitrile for PNC and 2.5 mL water and 2.0 mL ethanol for PNE. Poly(ethylene glycol) bis(2-bromoisobutyrate) (50 mg, 7.9 µmol), CuBr (4.5 mg, 31 µmol), CuBr$_2$ (4.7 mg, 21 µmol), NIPAM (264 mg; 2.3 mmol) and either HPMA-Boc-Cys(Acm) (67 mg, 0.16 mmol) for PNC or HPMA-ETSA (56 mg, 0.16 mmol) for PNE were dissolved in the corresponding polymerization solvents. The mixtures were deoxygenated by flushing with nitrogen for 15 minutes at room temperature and 15 minutes in an ice bath. Subsequently, 16 µL (60 µmol) of tris-[2-(dimethylamino)ethyl]amine (Me$_2$TREN) as copper ligand was added to the polymerization flasks. The reaction mixtures were stirred for 2 and 5 hours in the ice bath for the synthesis of PNC and PNE, respectively. The crude products were purified by dialysis of the reaction mixtures in water to 15 mL, followed by dialysis (MWCO, 10 kDa) against water at room temperature for two days and subsequently lyophilized. The obtained polymers were characterized using ($^1$H-NMR and GPC analysis. Acetamidomethyl (Acam) and tert-butylxycarbonyl (Boc) protecting groups of cysteines (in PNC polymer) were removed as described before. Briefly, Boc protecting groups of cysteines were removed by dissolving 250 mg of the protected PNC in dry DCM and trifluoroacetic acid (TFA) (1:1 v/v, 10 mL) and stirred for 1 hour at room temperature. Next, the solvent was evaporated under reduced pressure and the crude product was dissolved in 2 mL DCM followed by precipitation in 60 mL of cold diethyl ether. The Acm protecting group of cysteines was removed by dissolving 250 mg of the Boc deprotected polymer in a mixture of methanol (MeOH) and water (1:1 v/v, 10 mL) under a nitrogen atmosphere. Next, 500 µL HCl (1 M) and 1 mL iodine 0.2 M in
MeOH were added and left to react while stirring for 1 h at room temperature. Subsequently, 1 mL of ascorbic acid (1 M) in water was added to the reaction flask to quench the excess of iodine followed by addition of excess of tris(2-carboxyethyl)phosphine (TCEP) (250 mg) to reduce the formed disulfide bonds and the reaction mixture was subsequently stirred overnight. Finally, the mixture was dialyzed against water for 2 days at room temperature (MWCO, 10 kDa) and the final product was obtained after lyophilization and characterized by 1H-NMR and GPC.

2.2.2. NMR spectroscopy analysis. The obtained polymers were characterized by 1H-NMR using a Bruker 600 UltraShield spectrometer (Billerica, Massachusetts, USA). The chemical shifts were calibrated against the residual solvent peak of CHCl₃ (δ = 7.26 ppm).

2.2.3. Gel permeation chromatography (GPC). The molecular weights and molecular weight distribution of the synthesized polymers were determined using a Waters 2685 Alliance 2414 System (Waters Corporation, Milford, MA) equipped with a refractive index detector. Samples were dissolved in DMF containing 10 mM LiCl at a concentration of 5 mg mL⁻¹ and separation was carried out by 2 PLgel 5 μm Mixed-D columns (Polymer Laboratories, UK) in series at a temperature of 65 °C using the same solvent as mobile phase. The flow rate was 1 mL min⁻¹ and a series of linear PEGs with narrow and defined molecular weights were used as calibration standards. Data were recorded and analyzed with Empower software v.3, 2010.

2.2.4. Determination of cloud point of PNC and PNE. The cloud point (CP) of the synthesized polymers was determined using a Jasco FP-8300 spectrofluorometer (JASCO, Tokyo, Japan). The polymers were dissolved at a concentration of 1 mg mL⁻¹ in PBS (0.13 M NaCl, 2.7 mM KCl and 11.9 mM phosphates, pH 7.4). The temperature was ramped from 10 to 50 °C at 1 °C min⁻¹ and the measurements were performed at 650 nm. The CP was taken as the onset of increasing scattering intensity.

2.3. Micelle preparation and characterization

2.3.1. Preparation of the core crosslinked flower-like micelles. To form micelles, PNC and PNE were dissolved separately in PBS (0.13 M NaCl, 2.7 mM KCl and 11.9 mM phosphates, pH 7.4) at a concentration of 10 mg mL⁻¹ and left at 4 °C for 3 hours. Subsequently, the polymer solutions were mixed in a 1:1 volume ratio (i.e. 1:1 molar ratio of HPMA-Cys to HPMA-ETSA) and heated to 50 °C using an oil bath. The mixture was stirred at 50 °C overnight. The resulting micellar dispersion was dialyzed against water (MWCO, 10 kDa) for two days at room temperature and subsequently lyophilized.

2.3.2. Labeling micelles with a fluorescence probe. Micelles were prepared as described in Section 2.3.1. Subsequently, the buffer medium was refreshed, and the micelles were purified by PD-10 desalting columns equilibrated with PBS (0.13 M NaCl, 2.7 mM KCl and 11.9 mM phosphates, pH 7.4) according to the protocol provided by the supplier. Next, 10 μL of a 50 mg mL⁻¹ Viscous Blue 420 Maleimide stock solution in DMSO was added to 1 mL micellar dispersion and left to react at 4 °C for two days under a nitrogen atmosphere. Next, the labeled micelles were purified three times by PD-10 desalting columns equilibrated with PBS to remove non-conjugated dye.

2.3.3. Dynamic light scattering. The radius of micelles at different temperatures was measured at a concentration of 3 mg mL⁻¹ in PBS (0.13 M NaCl, 2.7 mM KCl, and 11.9 mM phosphates, pH 7.4) using an ALV7004 correlator, ALV/LSE-5004 Goniometer, ALV/Dual High QE APD detector unit with fiber splitting device with a set-up of 2 off detection system (Langen, Germany). A Uniphase Model 1145P He–Ne Laser was used at a laser wavelength of 632.8 nm and power of 22 mW. The measurements were performed at only 90° angle. The particle size was determined from the diffusion rate based on the Stokes Einstein equation. The temperature was increased from 10 to 40 °C with 10 minutes equilibration time at each temperature. The temperature was controlled by a Julabo CF41 (Seelbach, Germany) thermostatic bath and changes in viscosity were taken into account by the software.

2.3.4. Zeta potential. The prepared micelles in PBS were diluted (1:20 v/v) in HEPES (20 mM, pH 7.0) to a final concentration of 0.5 mg mL⁻¹ and the zeta potential was measured at 10 and 40 °C using a Zetasizer Nano Z (Malvern Instruments Ltd, Malvern, UK).

2.3.5. Fluorescence intensity measurements. The fluorescence intensity of dye-conjugated micelles was measured using a Jasko FP-8300 (JASKO, Tokyo, Japan) spectrofluorometer; the excitation and emission wavelengths were set at 320 and 400 nm, respectively. Micelles were dispersed at a concentration of 3 mg mL⁻¹ in PBS (0.13 M NaCl, 2.7 mM KCl and 11.9 mM phosphates, pH 7.4) and heated from 10 to 40 °C. Samples were allowed to equilibrate at each temperature for 10 minutes before measurement.

2.4. Micelle dispersion preparation and characterization

2.4.1. Preparation of dense micellar dispersions. Lyophilized micelles were dispersed in PBS (0.13 M NaCl, 2.7 mM KCl and 11.9 mM phosphates, pH 7.4) at concentrations of 7.5, 10, 12.5, 15, 20, and 30 wt% and left to hydrate for 3 hours at 4 °C prior to the measurement. For instance, a sample at a concentration of 20 wt% was prepared by dispersing 200 mg of lyophilized micelles in 800 μL of PBS. Details of the preparation of individual samples are provided in ESI,† Section S2, SI-Table 2.

2.4.2. Rheological characterization of dense micellar dispersions. Rheological analyses of dense micellar dispersions were performed on a DHR-2 rheometer (TA Instruments, New Castle, DE) using a 20 mm aluminum cone (1°) geometry equipped with a solvent trap. Temperature sweeps were performed from 40 to 10 °C at 1 °C per minute steps with a 30 second equilibration time for each temperature. The temperature was regulated through a Peltier Plate temperature control. The measurements were conducted at a fixed frequency of 1 Hz and a strain of 1% and the sample volume was 70 μL.
The yield stress measurements were performed using 12.5 and 30 wt% dispersions, at temperatures of 10 and 40 °C, respectively. The samples (70 µL) were subjected to a strain sweep from 1 to 40% at oscillation frequency of 1 Hz.

### 3. Results and discussions

#### 3.1. Polymer synthesis and characterization

Fig. 1 shows the structures of polymers investigated in this study synthesized using atom transfer radical polymerization (ATRP). As reported previously, PNE and protected PNC were obtained by copolymerization of NIPAM/HPMA-ETSA and NIPAM/HPMA-Boc-Cys-(Acm), respectively. The feed molar ratio of the monomers in both polymerizations was 93:7 and a poly(ethylene glycol) bis(2-bromoisobutyrate) with a number-average molecular weight (Mn) of 6 kDa was used as bifunctional ATRP initiator. The protected PNC triblock copolymer was obtained with a yield of 94% and the Mn of the polymer was ~42 kDa as determined by 1H-NMR and ~69 kDa (PDI 1.5) by GPC analysis (Table 1). The purified PNE was obtained with a yield of 85% and had an Mn of ~41 kDa as determined by 1H-NMR and Mn of ~64 kDa (PDI of 1.8) as determined by GPC (Table 1). The difference in the recorded Mn’s by GPC and NMR analysis of these polymers can be ascribed to the presence of strong inter- and intramolecular hydrogen bonding in PNIPAM based polymers as reported before.

The incorporation of HPMA-Cys and HPMA-ETSA units in the thermosensitive domains of the polymers provides terminal cysteine and thioester functionalities that can be exploited for native chemical ligation (NCL). PNC underwent a deprotection procedure to remove Acm and Boc protecting groups to yield a polymer with free cysteine moieties. 1H-NMR analysis showed that the deprotection of cysteines indeed was successful and GPC analysis showed an Mn of ~72 kDa for the deprotected polymer. As expected, both polymers exhibited a cloud point of 34.1 °C for PNC and 29.2 °C for PNE due to the presence of thermosensitive PNIPAM-blocks and the obtained values were similar as reported before for similar polymers (Table 1).

#### 3.2. Micelle formation and characterization

Micelles were prepared following a previously reported method by mixing PNC and PNE solutions (10 mg mL⁻¹) at a volume ratio of 1:1 (i.e. molar ratio 1:1 for HPMA-Cys and HPMA-ETSA) followed by increasing the temperature to 50 °C. The close proximity of thioester and thiol functionalities in the micellar core induces native chemical ligation leading to the stabilization of the micellar structures (Fig. 2A). Fig. 2B shows the radius of the micelles as a function of temperature in a dilute dispersion (3 mg mL⁻¹) as measured by DLS. By varying the temperature from 10 to 40 °C, the radius of the micelles changed from ~48 to ~35 nm with an inflection point at approximately 28 °C, which is close to the LCST of both polymers. Static light scattering at 10 and 40 °C demonstrated that the micelle’s molecular weights (~15.5 × 10⁶ kDa) and aggregation number (Nagg) (~400) were equal within the experimental error confirming the formation of core cross-linked micelles. SLS data have been reported before for this type of micelles, but for sake of readability are also shown in SI-Table S1 (ESI) at the relevant temperatures here.

![Chemical structures of deprotected PNC and PNE.](image)

**Table 1.** Characteristics of the synthesized ABA triblock copolymers of (protected) PNC and PNE. Both ABA polymers contain PEG (6 kDa) as midblock, whereas the thermosensitive outer blocks are composed of either NIPAM and HPMA-ETSA (PNE) or NIPAM and HPMA-Boc-Cys-(Acm) (protected PNC). The feed molar ratios of NIPAM to HPMA-Boc-Cys-(Acm) and HPMA-ETSA were 93:7.

| Polymer       | Obtained molar ratio | [NIPAM] : [HPMA-Boc-Cys-(Acm)] | [NIPAM] : [HPMA-ETSA] | Mₙ (kDa) | Mₘ (kDa) | PDI | CP (°C) | Yield (%) |
|---------------|----------------------|---------------------------------|------------------------|----------|----------|-----|----------|---------|
| PNC           | 91:9                 | —                               | —                      | 42.1     | 69.1     | 1.5 | 34.1     | 94      |
| PNE           | —                    | 92:8                            | —                      | 40.9     | 63.9     | 1.8 | 29.2     | 85      |

* Determined by 1H-NMR. * Determined by GPC. * Cloud point of the deprotected polymer.
micelles displayed a ζ-potential of $-2.3 \pm 0.4$ and $-4.2 \pm 0.2$ mV at 10 and 40 °C, respectively, showing a slight negative charge of the micelles above and below the LCST, in line with findings for other pegylated polymeric nanoparticles.44

To visualize the shrinking of the micellar core due to dehydration of PNIPAM chains above the LCST, a rigidochromic fluorescent probe was used.38,45 Rigidochromic fluorescent probes are excited by absorbing a photon of a specific wavelength. After excitation, there are two possible pathways to deactivate the excited-state: non-radiative and radiative. The non-radiative pathway (non-fluorescent) results in rotation of a specific bond that prevents effective π conjugation in the molecule. When this pathway is hampered by confinement induced by molecular structural changes or enhanced viscosity of the environment, the probe is forced to follow the radiative pathway and emit light to the deactivated excited state.46 To this end, the maleimide functionalized rigidochromic dye (Viscous Blue 420 Maleimide39) was conjugated to free thiol groups in the micellar core remaining after native chemical ligation and/or to non-reacted cysteine moieties in the micellar core. This conjugation positioned the rigidochromic molecule as a confinement probe in the PNIPAM core of the micelles. The fluorescence intensity of dye conjugated micelles was monitored as a function of temperature (Fig. 2C). First, a decrease in the fluorescence intensity with increasing temperature from 10 to 25 °C was observed, as it has been observed before for this dye in aqueous solution which was attributed to the decrease in viscosity of water with temperature.37 Since the core in this temperature range (10 to 25 °C) is highly hydrated, the lower fluorescence intensity with increasing temperature can be explained by the low local viscosity in the micellar core. Interestingly, by further increasing the temperature from 25 to 40 °C, the fluorescence intensity did not further decrease but instead increased. Most likely, the dehydration of PNIPAM and accordingly shrinkage of the micellar core resulted in an increase in the confinement of the rigidochromic probes. Therefore, these molecules follow the radiative pathway which in turn resulted in an increase in fluorescence intensity. Fig. 2D shows the change in fluorescence intensity as a function of the radius of the micelles. From 10 to 25 °C, when the radii are hardly changed (from 47 to 45 nm), a decrease in fluorescence intensity from 680 to 590 a.u. was observed as explained above. With decreasing the radius from 45 to 35 nm (from 25 to 35 °C) a significant change in intensity from 590 to 850 a.u. was observed, which shows that indeed shrinkage of micelles due to the dehydration of PNIPAM chains increased dye confinement and consequently increased dye intensity. Subsequently, when the radius of the micelles remained relatively constant, (35.7 to 35.0 nm) at a temperature from 35 to 40 °C, fluorescence intensity slightly decreased again, which indicates a slight decrease in viscosity of the dye microenvironment. According to Wu et al. PNIPAM based nanoparticles retain water (~70%) in their hydrophobic core even in a highly collapsed state at temperatures above the LCST.18 Therefore, probably a decrease in the viscosity of water in the micellar core upon increasing temperature resulted in an overall decrease in the viscosity of dye microenvironment, which led to a slight decrease in dye intensity.
3.3. Rheological characterization of dense micellar dispersions

The rheological properties of dense micellar dispersions were investigated as a function of temperature. The number of micelles (n) in different dispersions was calculated based on the concentration of samples and the molecular weight of the micelles (the details are shown in ESI† Section S2, SI-Table 2). This number was used to calculate the total volume of micelles (V_m) in each dispersion based on the radius of the micelles in a dilute dispersion (3 mg mL⁻¹). In addition, an effective volume fraction (i.e. packing fraction) \( \phi = V_m/V_t \) is defined, where \( V_t \) is the volume of a micelle dispersion (see ESI† Section S2, SI-Table 2).

The calculations show that the total volume of micelles (V_m) at concentrations \( \geq 7.5 \text{ wt\%} \) and at 10 °C is larger than \( V_t \) (SI-Table 2, ESI†). This indicates that the effective volume fraction (\( \phi \)) can be even above the maximum random packing fraction for monodisperse hard spheres \( \phi_{\text{top}} \approx 0.64^{20,21} \) possibly due to compressible deformation of the relatively soft micelles. Consequently, at the same temperature the volume of a given micelle in a dilute dispersion is larger than its volume in a concentrated dispersion as visualized schematically in Fig. 3.

The storage modulus (\( G' \)) of several micellar dispersions was measured while the temperature was increased from 10 to 40 °C (Fig. 4A). The sample at a concentration of 7.5 wt% displayed a low \( G' \) of \( \sim 10 \text{ Pa} \) with \( \tan \delta \approx 0.85 \) at 10 °C. By increasing temperature to 40 °C, this sample displayed a liquid state (\( \tan \delta \approx 4 \)). Below the LCST (10 °C), samples at concentrations of 10, 12.5, and 15 wt% showed \( G' \) values of \( \sim 700, 3000, \) and 6000 Pa, respectively with \( \tan \delta \approx 0.05 \), demonstrating solid-like behavior with a concentration dependent \( G' \). By increasing the temperature above the LCST (40 °C), the \( G' \) values decreased significantly to about a few pascals (<2 Pa) with \( \tan \delta \approx 1 \), indicating a transition from solid-like to liquid-like. The samples with 20 and 30 wt% micelles exhibited substantial \( G' \) values of \( \sim 17000 \) and \( \sim 28000 \text{ Pa} \), respectively, with \( \tan \delta \approx 0.05 \) below the LCST (10 °C). At temperatures above the LCST (40 °C), their \( G' \) decreased to \( \sim 150 \text{ Pa} \) (\( \tan \delta \approx 0.5 \)) and \( \sim 3000 \text{ Pa} \) (\( \tan \delta \approx 0.2 \)), respectively, meaning that no transition to liquid-like behavior had occurred.

The temperature dependency of storage modulus for micellar dispersions differing in concentrations can be described by critical-like behaviour: \( G' \sim (T_c - T)^{\gamma}^{47,48} \) in which \( T_c \) is the critical temperature and \( \gamma \) is the critical exponent. The critical temperature \( T_c \) is set at 28 ± 0.5 °C as evidenced from the sharp decrease in the experimental values of \( G' \) in samples with 10, 12.5, and 15 wt% (Fig. 4A). The critical temperature is the same for different concentrations considering 0.5 °C error in measuring the temperature. This temperature coincides with the inflection point of the size–temperature curve in Fig. 2 and is close to the LCST of PNC (~34 °C) and PNE (~29 °C). The solid curves in Fig. 4A show the best fits of the above equation to data points of samples 10, 12.5, and 15 wt% with a fixed \( T_c = 28 °C \) and yielded \( \gamma \) values of 2.1, 1.6, and 1.3 (all with an absolute error of ~0.1), respectively. This demonstrates that the critical exponent \( \gamma \) decreases with increasing concentration of the samples. Below the critical temperature, the core of micelles is hydrated, which results in an increase in micelle size (~35 nm vs. ~48 nm at 40 and 10 °C, respectively, Fig. 2B). Consequently, micelles were jammed together (\( \phi \geq 1.8 \)) and formed a colloidal glass with a substantial value of \( G' \). Increasing temperature above \( T_c \) and consequent reduction in the size of micelles resulted in a decrease in the effective volume fraction (\( \phi \leq 1 \)), and thus the average number of neighbors in direct contact with each other decreases\(^{31} \) resulting in a lower \( G' \) value and also in flow (\( \tan \delta \geq 1 \)). This observation suggests that \( \phi \) is the sole parameter controlling the rheological properties of the system. The samples with concentrations of 20 and 30 wt% did not show a sharp transition at 28 °C but represented a solid-like behavior above and below this temperature. This is due to the fact that at these concentrations \( \phi \) values are so high (1.4 \( \leq \phi \leq 5.6 \)) that the reduction in the size of micelles is not significant enough to result in a glass-liquid transition (\( \tan \delta \leq 0.5 \) below and above \( T_c \)). Therefore, the reduction in the size of micelles only reduces the extent of compression of micelles into each other which results in a lower \( G' \) and a higher \( \tan \delta \) above \( T_c \) (e.g. micellar dispersion 20 wt% displayed a \( G' \) of 150 (\( \tan \delta \approx 0.5 \)) and 17 000 Pa (\( \tan \delta \approx 0.05 \)) at 40 and 10 °C, respectively).

Fig. 4B shows \( G' \) as a function of \( \phi \) for micellar dispersions of different concentrations and temperatures. This figure shows that data points of different samples coincide on a master curve demonstrating that \( \phi \) is the sole parameter controlling the transition behavior of the system. As shown in this figure, \( G' \) substantially increases at a \( \phi \) of ~1.2 (black arrow) above which the system shows solid-like behavior with \( 0.05 \leq \tan \delta \leq 0.85 \). To quantitatively link the sharp transition of \( G' \) to \( \phi \), a disordered lattice model for hard-sphere colloidal glasses was used that gives the non-affine expression of the storage modulus as \( G' \sim \phi(z - z_c) \), in which \( z \) is the average number of neighbors of one micelle in the dispersion (coordination number)\(^{31,32} \) and \( z_c = 4 \) is the critical number at the glass transition when \( \phi = \phi_c \). \( \phi_c \) is the critical volume fraction at which the glass transition occurs. According to Zacccone et al.,\(^{31} \) \( \phi \) and \( z \) are related via \( z - z_c = (\phi - \phi_c)^{\beta} \), therefore it reads \( G' = kp(\phi - \phi_c)^{\gamma} \). The exponent \( b \) depends on the micelle-micelle interaction, including steric contributions. The best fit with three fitting parameters to the data points of Fig. 4B, yields the fitting parameters \( b = 0.98, k = 1821 \text{ Pa} \) and \( \phi_c = 1.31. \) \( b = 1 \)

Fig. 3 (A) Micelles in a dilute dispersion (B) compression of micelles in a concentrated dispersion.
indicates that $\varphi$ and $z$ are linearly proportional. By fixing the exponent $b$ at one, $k = 1769$ Pa and $\varphi_c = 1.31$ will be achieved as shown by the solid black curve in Fig. 4B. In addition, $b = 0.5$ has also been used in the literature for describing mechanical properties of soft micro particle systems. By fixing the exponent $b$ at 0.5 and fitting the data using the above function $k = 2584$ Pa and $\varphi_c = 1.2$ will be achieved. The result of this fit is shown by the red solid curve in Fig. 4B. As it is shown in Fig. 4B, $b = 1$ provides a better description of all the experimental data while $b = 0.5$ describes the behavior of the highest concentration (30%) series. Although our model predicts well the behavior of the system at high volume fractions, however, at lower volume fractions ($\varphi < 1.3$) it cannot capture well the straight evolution of $G'$. In the literature, an exponential growth is observed for increasing $G'$ as a function of the volume fraction for the low volume fractions ranges which can be explained by the Doolittle equation. This exponential model might predict the evolution of $G'$ at lower volume fractions in our system.

Furthermore, data of Fig. 4B show that the two high concentration micellar dispersions display $1.4 \leq \varphi \leq 5.6$ over the whole temperature range which is well above $\varphi_c$. Therefore, these two samples only display solid state behavior above and below $T_c$ and do not exhibit a transition from solid- to liquid state.

The behavior of our micellar system is in contrast with previous studies on PNIPAM microgels. For example, Weitz et al. observed that a dense dispersion of PNIPAM microgel particles (radius of 260 nm at $41{\degree}C$) first showed a glass transition and then after liquefication formed a gel upon an increase in temperature above the LCST which is ascribed by the authors to the formation of stable clusters of aggregated PNIPAM microgels above the LCST. The different behavior of the micelle dispersion system described in this study compared to the previous microgel systems could be attributed to the presence of the PEG corona that covers the micelles. Hence, above the LCST the hydrophilic PEG corona is exposed (SI-Fig. 1, ESI†), which avoids hydrophobic interactions between the dehydrated and hydrophobic PNIPAM cores and consequent particle aggregation. Besides, the slightly negative zeta potential ($-4.2 \pm 0.2$ mV) may also contribute to the stability of the dispersions of micelles by preventing their aggregation due to charge repulsion.

A similar observation was made for micelles based on poly(ethylene oxide)–polystyrene–poly(ethylene oxide) trilock

![Fig. 4](image_url)  
**(A)** Storage moduli ($G'$) of micellar dispersions as a function of temperature and for different concentrations in PBS. The solid curves are the best fit of $G' \sim (T_c - T)^b$ to the data of samples with concentrations 10, 12.5, and 15%. (B) $G'$ as a function of effective volume fraction ($\varphi$) at different micellar concentrations at different temperatures. The solid curve is the best fit of $G' \sim \varphi(\varphi - \varphi_c)$ with $\varphi_c = 1.31$.

![Fig. 5](image_url)  
**(A)** Total volume of micelles ($V_m$) as a function of concentration at 10 and 40 ℃. $V_m$ for each dispersion was calculated based on the radius of micelles in a diluted micellar dispersion (3 mg mL⁻¹) (see SI-Table 2, ESI†). (B) $G'$ as a function of the concentration of micellar dispersion for the two temperatures.
copolymers in ionic liquids, where increasing the concentration led to the formation of a soft elastic material with a reduced nanoparticle size attributed here to compression of the PEG corona.54

To clarify the storage modulus dependency on \( \varphi \) shown in Fig. 4B, \( \operatorname{G}' \) of six dispersions of different concentrations of 7.5, 10, 12.5, 15, 20, and 30 wt% at 10 and 40 °C were compared. Fig. 5A shows the total volume of micelles \( (V_m) \) for each sample which increases linearly with concentration. As expected, the slope is higher for samples at 10 °C than at 40 °C due to the hydration of the PNIPAM chains in the micellar core. A horizontal dashed line in Fig. 5A shows that \( V_m \) of the 12.5 wt% dispersion at 10 °C (2.2 mL) is very close to \( V_m \) of 30 wt% dispersion at 40 °C (2.1 mL) (SI-Table 2, ESI†). According to the model presented in Fig. 4B it is expected that these two samples display similar \( \operatorname{G}' \) although their concentration and temperatures are very different. Fig. 5B shows that \( \operatorname{G}' \) of the 12.5 wt% micellar dispersion at 10 °C (~2600 Pa) is indeed very close to \( \operatorname{G}' \sim 2400 \text{ Pa} \) found for the 30% sample at 40 °C (horizontal dashed line in Fig. 5B). These results indicate a concentration-temperature equivalence principle in our system.

Yield stress is an important parameter for materials that need to undergo extrusion processes such as 3D-printing. Fig. 6A shows that a micellar dispersion with a concentration of 20 wt% can be easily extruded through a nozzle even below the \( T_c \). When the applied stress is larger than the yield stress of the material, the dispersion flows and can thus be extruded. However, after extrusion when the applied stress is below the yield stress the material retains its shape and shows solid-like behavior.55 To investigate the yield behavior of the micellar dispersions, amplitude sweep rheology measurements were performed on micellar dispersions of 12.5 and 30 wt% concentrations. In Fig. 6B, \( \operatorname{G}' \) and \( \operatorname{G}'' \) are shown as a function of applied stress for the two samples with the same packing fraction \( \varphi \sim 2.2 \) at different concentrations and temperatures. Both samples show similar \( \operatorname{G}' \) and \( \operatorname{G}'' \) values at low shear stresses (linear regime). For both samples, with increasing stress, \( \operatorname{G}' \) drops and becomes comparable to \( \operatorname{G}'' \sim 660 \text{ Pa} \) at a stress of about 220 Pa (with an oscillation frequency of 1 Hz). This point is known as the yield point of the material and the corresponding stress is called yield stress.55 Therefore, the samples with similar packing ratio not only show similar \( \operatorname{G}' \) and \( \operatorname{G}'' \) in the linear deformation regime but also display the same yield stresses, and equivalent rheology behaviour in the nonlinear regime.

The rheology experiments were performed at a frequency of 1 Hz as frequency-independent behavior for \( \operatorname{G}' \) was anticipated when \( \varphi \) is above the critical \( \varphi \). Such behavior has been observed in similar systems composed of soft microparticle suspensions below the LCST.29 However, at high frequencies, deviations from the frequency-independent plateau may occur due to the rearrangement of packed particles.

4. Conclusion
In this study, the rheological properties of dense dispersions of flower-like micelles have been investigated. Temperature dependent change in the size of micelles resulted in formation of a colloidal glass with predictable storage modulus by changing the micelles’ concentration from 7.5 to 30 wt% at temperatures from 10 to 40 °C. When the storage modulus of different micellar dispersions at different concentrations and temperatures is plotted as a function of the effective volume fraction, the data points coincide onto a master curve. This indicates that the effective volume fraction of the micellar dispersions is the sole parameter controlling their rheological properties. Furthermore, the volume fraction induced glass transition in the system is described by a theoretical model indicating a critical volume fraction of 1.31, which is very close to the experimental value \( \varphi = 1.2 \). The observed transition from glass to liquid-like phase upon increasing temperature resembles upper critical solution temperature (UCST) behavior. Therefore, the developed system may find applications in fields requiring UCST polymers.

Conflicts of interest
There are no conflicts of interest to declare.
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