Thermal Conductivity of superconducting \((\text{TMTSF})_2\text{ClO}_4\): evidence for a nodeless gap

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We report on the first measurements of thermal conductivity in the superconducting state of \((\text{TMTSF})_2\text{ClO}_4\). The electronic contribution to heat transport is found to decrease rapidly below \(T_c\), indicating the absence of low-energy electronic excitations. We argue that this result provides strong evidence for a nodeless superconducting gap function but does not exclude a possible unconventional order parameter.

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The \((\text{TMTSF})_2X\) family of quasi-one dimensional conductors (the Bechgaard salts) are a well-known case of competition between superconducting and Spin-Density-Wave ground states \([1]\). At ambient pressure, most of these extremely anisotropic compounds undergo a metal-insulator transition at low temperatures and have a SDW fundamental state. Under moderate pressure, the SDW instability is suppressed and replaced by a superconducting transition at a critical temperature of the order of 1 K \([2]\). One exception to this scheme is \((\text{TMTSF})_2\text{ClO}_4\) which is superconducting at ambient pressure. The high-field properties of these compounds- including a particular version of quantum Hall effect \([3]\) and commensurability effects in the angular magnetoresistance \([4]\) - have been intensely studied during the past few years. However, in spite of early speculations on a possible unconventional nature of superconductivity in this context \([5]\), and contrary to the other families of exotic superconductors (i.e. Heavy Fermions and cuprates), the superconducting state has been subject to very few studies. The only attempt to explore the symmetry of superconducting order parameter in a Bechgaard salt is reported by Takigawa, Yasuoka and Saito \([6]\). These authors detected a \(T^3\) temperature dependence in the nuclear relaxation rate of proton in \((\text{TMTSF})_2\text{ClO}_4\) and concluded that the superconducting gap function should vanish along lines on the Fermi Surface.

Thermal conductivity has proved to be a powerful probe of gap structure in a number of unconventional superconductors. In the case of the heavy-fermion superconductor \(\text{UPt}_3\), thermal conductivity measurements constitute one major source of our current knowledge on the angular distribution of nodes in the gap function \([7,8]\). In the case of \(\text{YBa}_2\text{Cu}_3\text{O}_{6.9}\), several convincing signatures of \(d\)-wave superconductivity have been reported in a number of heat transport studies \([9]\). In the Bechgaard salts, measurements of thermal conductivity have been restricted to temperatures well above the superconducting instability \([10]\). In this letter, we present the first study of heat transport in an organic superconducting system. Our conclusion happens to be rather surprising as we find strong evidence for a nodeless gap.

![FIG. 1. Thermal conductivity divided by temperature for a relaxed sample of \((\text{TMTSF})_2\text{ClO}_4\). Superconductivity is suppressed by applying a small field along the \(c\)-axis. The lower insert presents the temperature dependence of the electrical resistance for the same sample. The upper insert shows the field dependence of \(\kappa\) for two different temperatures.]

The electrical and the thermal conductivities of four \((\text{TMTSF})_2\text{ClO}_4\) single crystals- grown by standard electrochemical technique- were measured with a conventional four probe method. Contacts were realized using silver paint on evaporated gold. Due to the poor...
conductivity of these contacts (~ 1Ω), the heat current passing through the sample was carefully checked using an Au-Fe thermocouple connected in series with the sample. The temperature gradient along the sample was measured with two RuO$_2$ thermometers which were thermally coupled to the contacts through gold wires. To reduce the heat loss, small solenoids of 50 µm superconducting Nb-Ti wires were made to hold each thermometer and measure its resistance. To test our apparatus, we used it to measure thermal conductivity of 20µm wires of metallic alloys (Al and Au-Fe) and found a linear thermal conductivity in agreement with the Wiedemann-Franz (WF) law and a Lorenz ratio very close to the Sommerfeld value ($L_0 = 2.45 \times 10^{-8} \Omega \text{m} \text{K}^{-2}$). All samples studied in this work showed jumps in resistance due to appearance of cracks during the cooling process. This has been regularly reported in transport studies of Bechgaard salts with silver-paint contacts and makes the determination of the absolute value of conductivity at low temperatures very difficult. However, the ratio of room temperature resistance to residual (i.e. $T \rightarrow 0$) resistance (RRR) was found to be very different from one sample to another. For slowly cooled samples (see below on the effect of cooling rate) this ratio was found to go from 10 to 440. Here we present the results for the sample with a RRR of 440 (dimensions: $1.1 \times 0.23 \times 0.07$ mm$^3$) which was most thoroughly studied. But the same basic features were observed for the three other samples.

Fig.1 shows the temperature dependence of $\frac{\rho}{T}$ and $\rho$ at low temperatures. The superconducting transition leads to a sudden decrease in $\kappa$ at $T \sim 1$K which is coincident with the end of the resistive transition. This kink in $\kappa(T)$ disappears with the destruction of superconductivity under a small magnetic field along the c-axis. The ratio of thermal and electrical conductances at the onset of superconductivity indicate that heat transport is dominated by phonons and that the electronic contribution counts only for a small fraction of total thermal conductivity for $T > 1$ K.

In general, the separation of lattice and quasi-particle components of thermal transport in superconductors is not straightforward, as the condensation of electrons in the superconducting state affects lattice contribution due to electron-phonon coupling. To gain insight on the effect of the superconducting instability on heat carriers, we plot in Fig.2, $\frac{\Delta \kappa}{T}$, the difference between the two experimental curves of $\frac{\rho}{T}$ (at H=0 and H= 5 kOe) as a function of temperature. As seen in the figure, upon the entry in the superconducting state, $\frac{\Delta \rho}{T}$ increases steadily with decreasing temperature before saturating at a temperature of about 0.4 K. This saturation has been observed at the same temperature for all the samples studied in this work and its value ($3.7 \pm 0.4 \mu \text{W} \text{K}^{-2}$ in this sample) was found every time to be close to $\frac{\Delta \rho}{T} = 3.8 \pm 0.5 \mu \text{W} \text{K}^{-2}$ here) which is the expected maximum electronic contribution to heat transport according to the WF law.

According to recent theoretical results [1], the separation of spin and charge degrees of freedom in an interacting 1D electron gas can lead to the violation of WF law and—in certain cases— to a divergence of Lorentz number at zero temperature. Here, the correlation between the zero-temperature extrapolations of normal state resistivity and the loss in electronic thermal conductivity constitute the first confirmation of the WF law in a quasi-one-dimensional conductor. This is not very surprising, since below the temperature scale defined by the interplane coupling $t_c$ (estimated to be a few Kelvins), (TMTSF)$_2$ClO$_4$ is expected to behave as an anisotropic 3D Fermi liquid. At finite temperatures, according to our data thermal conductivity exceeds the limit imposed by the WF law. But this additional thermal conductivity is within our experimental uncertainty on the absolute value of the Lorenz ratio. Moreover, cracks which have a less dramatic effect on thermal transport may cause a difference in the geometric factors for thermal and electrical transport. Therefore, at this stage, we will prudently remain within the boundaries of the WF law. Further studies of thermal transport in the normal state under higher magnetic field may elucidate this matter.

![FIG. 2. The difference between the thermal conductivity of (TMTSF)$_2$ClO$_4$ at H=5kOe and H=0kOe. Note the saturation at $T \sim 0.4$ K. The horizontal line (1) represents $\frac{\Delta \rho}{T}$, (2) schematizes a second scenario for temperature dependence of thermal conductivity in the normal state (see text).](image)

It can be shown that the saturation in $\frac{\Delta \kappa}{T}(T)$ constitutes a strong argument in favor of the absence of low-energy quasi-particle heat carriers. Neglecting the magnetoresistance (which is very small at 5kOe as seen in the insert of Fig. 1), one can express this difference as:

$$\frac{\Delta \kappa}{T}(T) = \left( \frac{\kappa_e^n(T)}{T} - \frac{\kappa_e^s(T)}{T} \right) + \left( \frac{\kappa_{ph}^n(T)}{T} - \frac{\kappa_{ph}^s(T)}{T} \right)$$

where subscripts (e, ph) stand for electronic and lattice components and superscripts (s, n) refer to superconducting and normal states. Now, a finite electron
phonon coupling would lead to an increase in the lattice conductivity in the superconducting state so that \( \kappa_{\text{ph}}^n(T) \leq \kappa_{\text{ph}}^s(T) \) for the whole temperature range below \( T_c \). This means that at any given temperature below \( T_c \), \( \frac{\Delta\rho}{\rho} \) constitutes an upper limit to the difference between the electronic conductivities of the normal and superconducting states. On the other hand, at zero temperature this difference is given by \( \frac{\kappa_n^c}{\kappa_s^c} \). These two constraints will allow us to extract the temperature dependence of normalized electronic thermal conductivity \( \frac{\kappa_n^c}{\kappa_s^c} \) from \( \frac{\Delta\rho}{\rho} \) and compare it to what is expected for different gap structures.

In Fig. 3., neglecting the effect of electronic condensation on lattice conductivity, we consider two different scenarios for the temperature dependence of thermal conductivity in the normal state. In the first hypothesis, a constant \( \frac{\kappa_n^c}{\kappa_s^c} \) (equal to \( \frac{\Delta\rho}{\rho} \)), is assumed. In the second scheme, we suppose that the thermal conductivity in the normal state follows the behavior imposed by the temperature dependence of electrical resistivity and the WF law (curve (2) in Fig. 2). The latter scenario implies a difference of 27 percent in the geometric factor of the sample for electric and thermal transport. As seen in Fig. 3, the normalized \( \frac{\kappa_n^c}{\kappa_s^c} \) curve is not very different for the two possible scenarios. It is instructive to compare them with the data on UPt3, the archetypical unconventional superconductor. The decrease in the electronic thermal conductivity within the entry in the superconducting state is much faster in \( (\text{TMTSF})_2\text{ClO}_4 \), for example, quasi-particle conductivity drops virtually to zero in \( (\text{TMTSF})_2\text{ClO}_4 \), but remains a sizeable (0.38) fraction of normal state conductivity in UPt3. Interestingly, our data are much closer to the predictions of the conventional Bardeen-Rickayzen-Tewordt theory [12]. The BRT function was computed for different values of where \( \frac{\Delta(0)}{T_c} \), where \( \Delta(0) \) is the amplitude of the superconducting gap at zero temperature. The closest fit was obtained for \( \frac{\Delta(0)}{T_c} = 2.3 \). This strong-coupling value shall be compared with 1.9 which is what is expected from size of the jump in specific heat at \( T_c \) [13]. However, due to the neglect of electron-electron collisions in the BRT model, one can shall be cautious in a quantitative comparison. Note that a finite electron-phonon coupling would lead to an even sharper decrease in \( \frac{\kappa_n^c}{\kappa_s^c} \) below \( T_c \).

Thus, in spite of several simplifications to obtain the plots of Fig. 3, our main conclusion is a direct consequence of the saturation presented in Fig. 2 and remains quite robust: there is no plausible way to reconcile our data with a gap function vanishing on the Fermi surface.
residual resistivity-, the quenched state becomes insulating because of a SDW transition at 9K. The change in the low-temperature thermal conductivity, shown in Fig. 4, is remarkable. The thermal conductivity is dramatically reduced reflecting the sensitivity of lattice conduction to anion disorder.

One can estimate the phonon mean free path in different states using the classical phonon gas equation $\lambda_{ph} = \frac{1}{s_{ph} \nu_{s}}$, where $s_{ph} = \beta T^2$ is the lattice specific heat ($\beta = 58 \mu J/cm^2K^4$ [7], $\nu_{s}$ is the velocity of sound (3 km/s is the reported value [15] for (TMTSF)$_2$PF$_6$ along the a-axis) and $\lambda_{ph}$ is the mean free path. In this picture, the $T^2$ dependence of thermal conductivity in the quenched state, indicates that the phonon mean-free-path increases very slowly with decreasing temperature and can be estimated to be about 14µm at 400mK. This is one order of magnitude smaller than the maximum allowed by the sample dimensions (∼ 150 µm) and suggests that the disorderly domains of anion ordering in the quenched state [14] strongly scatter phonons. On the other hand, in the relaxed state, where the thermal conductivity shows an essentially $T^2$ behavior below $T_c$, the phonon mean-free path is estimated to be 100µm at 200mK. The ballistic regime and the associated cubic behavior in thermal conductivity is only expected below 130 mK. Note that the effect of cooling rate on heat transport confirms the smallness of electron-phonon scattering. Indeed, in the quenched state, the phonons are much more affected by anion disorder than the absence of electrons as scatterers.

The main outcome of this work is that the superconducting gap of (TMTSF)$_2$ClO$_4$ has no nodes. This result is in contradiction with the conclusion of the only other experimental investigation of gap structure in this system [3]. One shall note, however, that the temperature range where the nuclear relaxation rate is reported to show a $T^3$ dependence is limited to $T > \frac{T_c}{2}$ [5]. This can not be considered as a convincing evidence for nodes in gap, as even for conventional superconductors, the exponential behavior is expected only at very low temperatures.

We would like to stress that a nodeless gap in this compound is not necessarily associated with s-wave superconductivity. Enumerating possible gap functions for a quasi-one-dimensional, Hasegawa and Fukuyama [17] showed that a pseudo-triplet (i.e., odd-parity) gap function with no nodes is possible in the context of Bechgaard salts (see the $t_2$ state in ref. [15]). Indeed, here the order parameter can have opposite signs for anti-parallel wave-vectors without vanishing anywhere on the Fermi surface, due to the openness of the latter. The strongest argument in favor of an odd-parity superconducting order parameter is the fascinating behavior of the upper critical field. A recent study by Lee et al. [15] on the sister compound (TMTSF)$_2$PF$_6$ has shown that when the magnetic field is oriented in the most-conducting plane, the upper critical field exceeds the Pauli limit. Insensitivity to this limit is naturally explained for Cooper pairs in a triplet state [5]. More studies are required to examine further this appealing possibility of an odd-parity gap function without nodes. From a theoretical point of view, it is highly desirable to establish all the possible gap functions for the Fermi surface of (TMTSF)$_2$ClO$_4$. Indeed, ref. [7] neglects triclinic symmetry of the crystal and the low-temperature shape of the Fermi surface after the opening of the anion-ordering gap.

In conclusion, we have measured the thermal conductivity of (TMTSF)$_2$ClO$_4$ in the superconducting, metallic and insulating states. The results are incompatible with the presence of nodes in the superconducting gap function. Moreover, electrons are found to have little effect on heat conduction by phonons.

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