1. Introduction

In recent years, content-based retrieval has emerged as an important topic for research, as well as an increasingly powerful reference tool for the general public. Services known as reverse image search engines such as TinEye, Bing or Google Image Search are able to quickly sift through vast quantities of images to return those most similar to a picture submitted by their users. This search modality truly captures the visual content of the query, and can be used to quickly collect rich information on any object or scene encountered, to a degree unachievable by the conventional text-based method.

A reference tool of this caliber based on video, which is a much more informative medium than static image data, could provide similar convenience and versatility in the context of laparoscopic surgery. Useful post-operative applications include surgical training, in order to find cases of interest to study; or reporting and patient data indexing, in order to trace the history of incidents and other important landmarks in procedures. In practice, this can take the form of an interface displaying similar cases, refreshing search results automatically; this can be shown directly to surgeons in an operating room. Indeed, the process of hashing converts large data entries into compact binary arrays or hashes, enabling large-scale search operations at a very fast rate. However, due to fluctuations over the course of a video, not all bits in a given hash are equally reliable. In this work, we propose a method capable of mitigating this uncertainty while maintaining a light computational footprint. We present superior retrieval results (3-4 % top 10 mean average precision) on a multi-task evaluation protocol for surgery, using cholecystectomy phases, bypass phases, and coming from an entirely new dataset introduced here, surgical events across six different surgery types. Success on this multi-task benchmark shows the generalizability of our approach for surgical video retrieval.

Live Laparoscopic Video Retrieval with Compressed Uncertainty

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Searching through large volumes of medical data to retrieve relevant information is a challenging yet crucial task for clinical care. However the primitive and most common approach to retrieval, involving text in the form of keywords, is severely limited when dealing with complex media formats. Content-based retrieval offers a way to overcome this limitation, by using rich media as the query itself. Surgical video-to-video retrieval in particular is a new and largely unexplored research problem with high clinical value, especially in the real-time case: using real-time video hashing, search can be achieved directly inside of the operating room. Indeed, the process of hashing converts large data entries into compact binary arrays or hashes, enabling large-scale search operations at a very fast rate. However, due to fluctuations over the course of a video, not all bits in a given hash are equally reliable. In this work, we propose a method capable of mitigating this uncertainty while maintaining a light computational footprint. We present superior retrieval results (3-4 % top 10 mean average precision) on a multi-task evaluation protocol for surgery, using cholecystectomy phases, bypass phases, and coming from an entirely new dataset introduced here, surgical events across six different surgery types. Success on this multi-task benchmark shows the generalizability of our approach for surgical video retrieval.

Intraoperative use cases are even more interesting to consider for laparoscopy, due to the technically challenging nature of this type of procedure: for all its clinical benefits, such as decreased pain, shorter recoveries and decreased infection risks, operating with an unintuitive set of instruments and indirect vision can be a source of confusion and errors (Mascagni et al., 2020). Those can be alleviated by adequate reference tools: assuming a large enough database of recorded surgeries is available, quick navigation based solely on the video feed of the current procedure could provide reference extensive enough to cover any clinical scenario encountered. This would include unusual patient anatomies as well as rare incidents such as cases of severe bleeding, device failure or surgical errors; most interestingly, matching surgeries with adverse post-operative outcomes may be signaled to surgeons.

Yet, research on surgical activity understanding has only studied video retrieval to a very minor extent. Early work in this area consisted of a few studies involving handcrafted features and relatively small amounts of data (Droueche et al., 2014; Amanat et al., 2018). Other tasks explored similar concepts for visual queries in surgical video content (Iwianad et al., 2014; Funke et al., 2018; Petscharig and Schöffmann, 2018). Long after those, the one major study comes from Wang et al. (2022) as a research effort parallel to ours. The rest of surgical activity understanding is mostly focused on
recognition-based approaches, where computer vision algorithms explicitly name activities appearing in the current frame of the laparoscopic video feed, according to a pre-determined set of classes. For example, recent works have successfully trained classifiers to recognize surgical phases, steps and even individual actions. However this type of approach is by design quite narrow and rigid: a true reference tool, just like modern search engines, would be expected to insight on surgical video content richer than just a category it belongs to. Additionally, should a new event, object or activity require to be identified, a entirely new classifier needs to be trained, with new annotations.

Non-clinical computer vision research, on the other hand, did give attention to video retrieval with approaches based on deep video hashing [Liong et al. (2017); Zhang et al. (2016); Song et al. (2018); Li et al. (2019)]. This technique uses deep neural networks to extract compact binary representations or hashes from videos. Assuming the hashes reflect the visual content, they can be used to quickly find similar videos, even in very large databases. However, proposed approaches until recently presented a key limitation which conflicted with intraoperative use: no live video sources were ever considered.

This raises the first of several challenges posed by intraoperative video retrieval for laparoscopy. This particular application scenario, characterized by strict timings, would require a highly responsive and dynamic retrieval system. Assuming queries are performed with video clips from the laparoscopic stream that are long enough to be informative (~30s), displaying search results after the full duration of a clip - or even immediately at the end may not be enough. A true real-time search engine should be reactive enough to find relevant videos far before the end of the clip, anticipating for future content in order to adapt to real-time conditions. We refer to this as the live video retrieval task.

Video hashing, where the video content submitted as query is represented by a binary hash, adds another challenge. In this particular form of retrieval, nearest-neighbor search is performed based on the Hamming distance between hashes, i.e. the number of conflicting bits. The hash adapts to real-time conditions, with bits fluctuating based on the new content seen from the laparoscopic feed. For hashes in the database to search from, which are extracted at one particular point in time, the value of individual bits should be examined with caution when searching, with a method accounting for their uncertainty. Additionally, this method should add as little overhead as possible on top of hashing, whose main advantages are its speed and low space consumption.

Finally, an efficient retrieval method should be as general as possible. First, the training process should be unsupervised. More importantly, the search results also need to be clinically relevant from a wide variety of perspectives, and not just according to one particular set of labels. Assessing this quantitatively is a difficult issue, which has not yet been thoroughly addressed in the literature on video retrieval.

This work introduces a new triple benchmark for surgical video retrieval in surgery. The relevance of search results returned by the same model is measured according to:

- cholecystectomy phases, using the Cholec80 dataset
- bypass phases, using the Bypass40 dataset
- surgical events, with the CEV64 dataset

With relevant search results across this wide range of clinical semantics, this ensures the generality of our surgical video retrieval method.

The last dataset listed contains 10 types of intraoperative events found in 6 different types of surgery such as active bleeding or incising. As explained in Figure 3, each of these events carries specific risk factors making them particularly important to identify, emphasizing the importance of this type of study in the community moving forward.

The retrieval method proposed extends our previous work [Yu and Padoy (2020)], focused on non-clinical computer vision datasets; the technical contribution of this method enables retrieval during a video in real time, and uses anticipatory mechanisms to compensate for inaccessible future information. Now equipped with the ability to perform video retrieval from live sources such as a laparoscope, we add as technical contributions improvements that mitigate uncertain bits. We first formally define bit uncertainty from two perspectives, depending on the bit encoder employed. Accounting for both, we then define for each hash a combined uncertainty pattern, which is itself binary in order to limit its computational footprint. We decrease that same footprint even further with a compression technique based on combination ranking, and analyze the corresponding gains.

Our contributions can be broken down as follows:

1. We propose an unsupervised video hashing method compatible with live video sources, that uses anticipation for enhanced retrieval results
2. We introduce the problem of live video retrieval to the surgical domain
3. We introduce the concept of uncertainty in video hashing, then account for it using a new lightweight method to drive up video retrieval performance
4. We introduce a general benchmark for surgical video retrieval incorporating a wide variety of clinical semantics
5. We use retrieval to study surgical events, via the CEV64 dataset

2. Related work

Even though the problem at hand is new, the work presented in this paper connects to several other research areas, both clinical and non-clinical.

2.1. Early activity recognition

Methods presented in the computer vision community rarely factor in live conditions to a significant extent. The one subdiscipline where those play a major role is early activity recognition, where models observe an action in progress in a video and attempt to identify it before it ends. This severely cuts down the visual content available to the predictor, requiring approaches tailored to those challenging conditions instead of ordinary activity recognition methods. Additionally, evaluation requires a dedicated protocol, with inference
repeated either at various levels of observation - i.e. ratio of total video duration - or regular time intervals. One solution for early recognition is to increase the contribution of predictions made earlier in the video, as done by [Akbarian et al. (2017) with a time-modulated loss or [Hu et al. (2019) using time-based soft labels.

A different way to proceed is to attempt to synthesize content from the video’s future. [Rodriguez et al. (2019) and generate future frames using generative adversarial networks. Gammulle et al. (2019) use separate visual and temporal generative models to synthesize future frame embeddings.

Finally, teacher-student distillation methods rely on a pair of models; only one - the teacher - has access to all the frames, generating representations the other model - the student - then has to copy from a partial video. Kong et al. (2017) apply this principle to 3D CNN models, while [Wang et al. (2019) do so with a pair of LSTM models, bidirectional for the teacher and unidirectional for the student. The one existing study of early activity recognition in surgery falls into this category as well, with a teacher LSTM that is given access to a certain number of future frames [Kannan et al. (2020).

2.2. Video hashing

Retrieval by similarity is a long-standing problem in computer vision, with recent progress made through the combination of two techniques: deep neural networks, to convert data entries into vector representations that capture the original visual content; and hashing, to generate compact binary arrays or hashes from those representations to facilitate search. Single-image hashing has been the main focus in the literature; except for our method [Yu and Padoy (2020), the few works addressing video hashing do so from a static viewpoint, considering full videos only.

Pooling-based approaches [Liong et al. (2017); Wu et al. (2017); 2019] extract features from video frames, then binarize their temporal average. To improve the quality of the hash, geometric transformations [Wu et al. (2017); 2019] can be applied to the features.

Other methods offer more substantial temporal modeling: [Zhang et al. (2016)] used an encoder based on a differentiable binary LSTM unit, where the hash itself serves as the memory. Similar methods followed [Song et al. (2018); Li et al. (2019)], with variations on the same principle.

2.3. Surgical activity understanding

In recent years, surgical activity understanding has been dominated by deep neural networks solving classification tasks. Depending on how such tasks are defined, the resulting description of the activity taking place can be more or less granular.

The Cholec80 dataset was first introduced by [Twinanda et al. (2016a), to models capable of recognizing, among 7 existing surgical phases for laparoscopic cholecystectomy, the correct one. Subsequent works [Twinanda et al. (2016b); Jin et al. (2018); Hajj et al. (2018); Jin et al. (2020); Czempiel et al. (2020) proposed, for this same task and on the same dataset, increasingly refined models derived from the LRCN concept [Donahue et al. (2015): a convolutional neural network as a visual feature extractor, followed by a deep temporal model. Similar phase recognition studies using the CATARACTS dataset (Al Hajj et al. (2019) were conducted for cataract surgery.

Ramesh et al. (2021) introduced a new dataset and a finer level of granularity: Bypass40, with 40 videos of Roux-en-Y gastric bypass, provided step annotations in addition to phases. Finally, Nwoye et al. (2020) introduced the surgical action triplet recognition task on a subset of Cholec80, offering the most detailed description of surgical activity achieved so far.

2.4. Medical content retrieval

Retrieving information from medical databases is a research topic that has been actively explored in recent years, albeit on a smaller scale, with less challenging data and very rarely for surgery. Biomedical and diagnostic images have been the main areas of focus instead, involving various medical specialties and modalities. In radiology, Goldminer [Kahn and Thao (2007)] introduced an early concept of text-based search engine specifically for X-ray images. Content-based approaches using hashing followed later for chest X-ray [Conjeti et al. (2017); Chen et al. (2018).

Other types of images involved include MR, with [Gao et al. (2015)] using retrieval with multi graph learning for early diagnosis of Alzheimer’s disease, CT for liver lesions [Costa et al. (2011)] and ultrasound [Lin et al. (2009)] for liver, kidney and pelvis. Microscopy in biomedical research received the attention of several retrieval methods: [Gu et al. (2017); Mesbah et al. (2015); Peng et al. (2019)] targeted digestive tract endoscopy, neuron and histopathology images respectively, with the last two relying on hashing. Large databases spanning multiple modalities were used for research on content-based retrieval: the Yale Image Finder [Xu et al. (2008)] combined OCR with text-based search.

Stathopoulos and Kalamboukis (2012) used latent semantic analysis, while [Haas et al. (2011)] used interest points based on superpixels.

Surgery, in contrast, has only seen sporadic uses of retrieval or similar tasks. [Drouiche et al. (2014)] presented a content-based retrieval method for cataract surgery videos with handcrafted features, based on MPEG video encodings. Another approach with handcrafted features was introduced by [Amanat et al. (2018)] on videos of knee surgery. Looking at laparoscopic surgery specifically, true video retrieval works are almost non-existent: the one example available comes from research efforts parallel to ours [Wang et al. (2022)], with a video hashing method separating motion and background for retrieving clips from the Cholec 80 dataset. Intra-video task boundary retrieval as done by [Twinanda et al. (2014)], and frame attribution as featured in [Funke et al. (2018); Petscharnag and Schöffmann (2018) are the closest related work otherwise.

2.5. Position of our work

Deep hashing methods clearly stand out as the main direction in the current research on content-based retrieval, including in the medical field where image retrieval has been a
very active research topic across many specialties of medicine (Section 2.4). With the deep hashing method shown here, we continue in this direction with surgical videos, a challenging type of media overlooked by the current literature.

In contrast, from the standpoint of surgical activity understanding (Section 2.3), our work clearly departs from the current trend of explicit recognition which is currently heavily focused on refining the recognition task. Every new refinement requires new classes to be defined by clinicians, new annotations to be provided and new models to be trained and deployed. In that regard, retrieval methods, which are obtained independently of any activity class definitions in the unsupervised case, provide much more flexibility. This class-agnostic trait of retrieval is what we demonstrate with our multi-task benchmark.

Real-time aspects of video data are addressed in recognition problems (Section 2.1), but not in the more complex problem of retrieval (Section 2.2). Comparison of our method against existing video hashing works would only stand for static, full video observations. Instead, our experiments address the pending issues of the real-time case: searching from a live video source, anticipating the rest of a video query and accounting for hash variability over the course of a video - these constitute our work’s main technical contributions.

3. Methods

3.1. Overview

Figure 1 provides an overview of the approach: two hash function models, trained with self-supervision, read video clips and output binary codes as the video plays; the second does so in a way that predicts the missing content. For evaluation, performed on three separate test sets, each video clip from a database is read by the first model in its entirety, and mapped to its corresponding hash. During this process, fluctuations in each bit of the hash are observed; locations of uncertain bits are stored in an array, which is then compressed. The hash, along with its corresponding uncertainty pattern, are then stored together in the gallery or codebook. We search into this database using a separate set of video clips; hashes from a given surgical intervention appear in the query set, none of its clips appear in the codebook set and vice-versa.

Cholec80. The Cholec80 dataset Twinanda (2017), a classic benchmark in surgical activity recognition, is a subset of Endocorpus. Those are, among the available cholecystectomy videos, 80 annotated with surgical phases. Those 7 phases are presented in the supplementary material. 307 clips are used as queries, to search into a database of 908 clips.

Bypass40. 40 of Endocorpus’ gastric bypass videos are annotated with surgical phases as well, forming the Bypass40 dataset Ramesh et al. (2021). With 11 phases (see supplementary material, Section A) the workflow of this procedure is much more complex. The clip count is 284 for queries, and 1409 for the database.

CEV64. Multi-procedure datasets are scarce in the surgical computer vision community, with studies mostly focusing on one particular procedure. The purpose of CEV64 (Collected Events in surgery) is to study more general traits of laparoscopic surgery, with annotations for events found across several procedure types. In addition to a background class, we report 10 event categories, with details provided in Figure 5. Since all these events carry high clinical significance, retrieving them automatically could be particularly useful. The queries and the database contain 580 and 1659 clips respectively, both sampled evenly across event classes in order to counteract the imbalance shown in Figure 5.

3.3. Feature extraction

Visual feature extraction follows the same incremental sampling scheme we introduced in Yu and Padoy (2020). As shown in Figure 4, we use a spatio-temporal model: an I3D 3D convolutional neural network Carreira and Zisserman (2017) pretrained on the Kinetics dataset progressively reads the video in chunks of 32 frames or 1.3 s of video at 25 fps. Video chunks are consecutive, i.e. without overlap, so as to avoid redundancy. For each chunk, a 4096-D feature vector is generated, capturing the video’s fine-grained temporal dynamics. Unlike the original sampling scheme found in previous hashing studies Liong et al. (2017) Zhang et al. (2016)
Our approach uses an encoder built around a binary LSTM [Zhang et al. (2016)], generating hashes from the visual feature sequences extracted by I3D. This is nearly identical to a conventional LSTM, with two key differences: binarization operation is applied to the hidden state [6] turning it into a hash; this hash then serves as the LSTM’s state, and is updated as the video advances in order to account for the new content seen. The second major difference is in the backpropagation; gradients nullified by the binarization are replaced with a hardtanh artificial gradient. Training such a model can be done in an autoencoder-type setup (Figure 5). For instance in the SSTH-RT+ (Self-Supervised Temporal Hashing Real-Time Plus) baseline approach from our previous work (Yu and Padoy, 2020), the input sequence is first randomly truncated to a ratio or level of observation $\alpha$, then fed to the encoder. The final hash returned serves as a representational bottleneck; the decoder LSTM reads the hash and attempts to reconstruct the truncated sequence. This coaxes the encoder into incorporating as much visually discriminative information as possible.
into the hash. Additionally, truncating sequences ensures the encoder has seen incomplete videos, which are expected in real-time conditions; this truncation process is the distinctive trait of SSTH–RT+.

Using this as a starting point, a more advanced method for real-time retrieval can be proposed. When performing retrieval from a live video source, visual information from future frames is missing. LA–CODE or Look-Ahead Code, introduced in our previous work [Yu and Padoy 2020], counteracts this deficit by explicitly enforcing anticipation. This is a distillation method using two encoders: the first one, or primary, is trained with SSTH–RT+; we use it to encode database videos into the codebook. The second one, or secondary encoder is responsible for encoding query videos, which are incomplete in a real-time scenario. We initialize the secondary with the primary’s weights then train it further with an anticipation mechanism can be readjusted to account for uncertainty: consider a bit where the primary and the secondary often enter in conflict can be assumed to cause mismatches when querying, and should therefore be considered untrustworthy.

From now on, we will refer to those as type I uncertainty and type II uncertainty respectively (Figure 4). We provide a formal definition for these quantities in the following lines.

Considering a sequence of features representing a video clip $V = V_1, ..., V_T$ of duration $T$, we write the $t$–th subclip as $U_t = (V_1, ..., V_t)$. Assuming we use $d$ bits, let $P$ and $S$ be LA–CODE’s primary and secondary encoders. Then throughout the course of the video $V$, $P$ outputs the hash sequence:

$$P(U_1), P(U_2), ..., P(U_t), ... P(U_T).$$

$P(U_t)$ in particular is the one stored in the codebook. For any timestep $t$, the $i$–th bit in the primary’s hash is written as $P_i(U_i)$. $S$ for the secondary follows the same notation.

Type I uncertainty for video $V$ at bit $i$ is defined as follows:

$$p_i(V) = \frac{1}{T-1} \sum_{t=1}^{T-1} P_i(U_t) \otimes P_i(U_1).$$

$\otimes$ is the bitwise XOR operation. Concretely speaking, this is the fraction of the time the primary spends in disagreement with the hash stored in the codebook. By measuring how steady an individual bit remains over the course of the video, this value can be used as a measure of uncertainty as well. Type II uncertainty, on the other hand, is defined as:

$$s_i(V) = \frac{1}{T} \sum_{t=1}^{T} P_i(U_t) \otimes S_i(U_t).$$

Or, more simply, the fraction of the time the secondary spends disagreeing with the hash stored in the codebook. $p$ and $s$ can then be blended into a single uncertainty score, using a balance factor $\theta$:

$$\mu(V, \theta) = \theta \cdot p(V) + (1 - \theta) \cdot s(V).$$

Storing $\mu$ itself along with $P(U_T)$, however, would be an extremely disproportionate way of communicating uncertainty ($d$ floating-point values for $d$ bits; with 32-bit floats that would be a factor 32). A much more space-efficient way to proceed is, for a given bit skepticism level $K_{bs}$ (i.e., presumed number of untrustworthy bits in a hash), to flag the position of the $K_{bs}$ most uncertain bits:

$$\mathcal{F}(V, \theta, K_{bs}) = \Phi_{K_{bs}}(\mu(V, \theta)).$$

The $i$-th coordinate of $\Phi_{K_{bs}}(X)$ is 1 if $X_i$ is in $X$’s top $K_{bs}$ values, 0 otherwise. This is simply a binary mask suppressing non-top K entries.

With this information at our disposal, the querying mechanism can be readjusted to account for uncertainty: consider a query video $Q$ at time $t$, and a database entry $R$ to compare
it to. In LA-CODE, the Hamming distance $H$ would be computed as the number of conflicting bits between the query and the database entry’s representations. Assuming hashes of size $d$:

$$H(Q_i, R) = \sum_{i=1}^{d} P_i(R) \otimes S_i(Q_i),$$ (7)

Using the binary uncertainty $F$ and a discounting factor $\gamma$, we can modulate the contribution of each bit in the sum:

$$\Delta(Q_i, R, \gamma) = \sum_{i=1}^{d} [P_i(R) \otimes S_i(Q_i)] \cdot (1 - \gamma \cdot F_i(V, \theta, K_{bs})).$$ (8)

In summary, our new method, which we will refer to as UL-ÇODE for Uncertain LA-CODE, performs the following steps:

- compute Type I and Type II uncertainty values $P, S$
- blend the two using a balance factor $\theta$
- flag the position of the top $K_{bs}$ uncertain bits
- when querying, discount uncertain bits in the hamming distance computation by a factor $\gamma$

The 3 free hyperparameters of the method are the discounting factor $\gamma$, the balance factor $\theta$, and the bit skepticism level $K_{bs}$.

### 3.6. Computational footprint of uncertainty awareness

Accounting for bit uncertainty during retrieval comes at a certain cost, both in terms of time and space. With execution speed and compactness both being key advantages of hashing, it is crucial that the impact of our upgrades on the overall computational footprint is kept at a minimum in order to preserve scalability.

This is formalized by the two following constraints:

1. **Redundancy limit**: the additional space consumed remains strictly under $dN$ bits (i.e. the size of the original codebook)

2. **Speed conservation**: the number of additional bit operations required per query is small compared to $dN$ (the number of xor operations for hamming distance computations required in the original algorithm)

**SSTH-RT+**, a greedy baseline presented in Yu and Padroy (2020), evidently contradicted both; with $n_{dupl}$ truncated duplicates, both the space consumption and the number of operations were multiplied by $n_{dupl}$. Careless tampering with the codebook purely for the sake of retrieval performance can therefore severely undercut computational performance. We propose a method for avoiding this with UL-ÇODE.

We first examine the redundancy limit constraint. Communicating the position of $K_{bs}$ uncertain bits in an array of $d$ bits can trivially be done with another $d$-bit array acting as a binary mask, set at 1 at uncertain bit positions. Doing so for each of the $N$ codebook therefore requires $d \cdot N$ additional bits - exactly the limit. However keeping the space consumption strictly underneath is possible by **compressing the uncertainty pattern**.

The number of possible binary masks of $d$ bits is of course $2^d$. Yet, among those, we only need to account for the ones with a predetermined number $k = K_{bs}$ of bits set to 1. This drops the number of possibilities to the number of $k$-combinations of $d$ elements, also known as the binomial coefficient $\binom{d}{k} = \frac{d!}{k!(d-k)!}$. Encoding an uncertainty pattern for $k$ bits therefore only requires $d_u = \log_2 \binom{d}{k}$ bits instead of $d$. Comparing these two values to evaluate the corresponding space gain is not straightforward - we provide examples in Table 1.

However we are able to provide a lower bound for the number of bits we are able to save:

$$d - \log_2 \binom{d}{k} \geq \frac{1}{2} \log_2 \left( \frac{\pi \cdot d}{2} \right).$$ (9)
Table 1. Selected examples for $\log_2(\binom{d}{k})$; $d$ indexes rows, $k$ is expressed as a ratio of $d$ in each column.

| $k$ | $\log_2(\binom{d}{k})$ | $k$ | $\log_2(\binom{d}{k})$ | $k$ | $\log_2(\binom{d}{k})$ | $k$ | $\log_2(\binom{d}{k})$ |
|-----|----------------|-----|----------------|-----|----------------|-----|----------------|
| $\frac{d}{8}$ | 8 | 96 | 2 | 32 | 128 | 4 | 64 |
| $\frac{d}{4}$ | 12 | 192 | 4 | 64 | 192 | 8 | 128 |
| $\frac{3d}{8}$ | 16 | 256 | 8 | 128 | 256 | 16 | 512 |
| $\frac{d}{2}$ | 24 | 384 | 16 | 256 | 384 | 32 | 1024 |

Fig. 8. Uncertainty pattern compression. Each 7-bit pattern of two uncertain bits can be assigned a rank from 0 to $\binom{d}{2} = 5$; for example by using the lexicographic order. This rank is then written in base 2. In this case this saves two bits over the original pattern.

A proof sketch for this result is given in the supplementary material, section E.

Practically speaking, any of the $2^{d_k}$ binary masks of $k$ uncertain bits can be indexed by a binary array of size $d_k$; we propose to do this using the lexicographic order position written in base 2 (Figures 8).

Storing this compressed mask instead of the mask itself preserves space - however restoring the mask using its index is not trivial: this is referred to as the combination unranking problem.

For very low values of $k$, one can maintain a look-up table during retrieval. Looking up a mask costs $O(1)$; space complexity, however, is $C_s = d \cdot \binom{d}{k}$ bits. In the worst case of $k = \frac{d}{2}$, we can use Stirling’s approximation to gauge this quantity:

$$C_s \approx 4^d \sqrt{\frac{d}{\pi}}$$

This is roughly exponential; to provide one example, a look-up table for uncertainty patterns of 48 bits in arrays of 96 bits would approximately consume $3.5 \cdot 10^{38}$ bits of memory ($4.3 \cdot 10^{43}$ TB). For this reason, algorithms for unranking combinations on the fly have been developed. Notably, Donnot et al. Genitrini and P´epin (2021) proposed a fast algorithm named unranking_factoradic with $O(d^2 \cdot \log_2(d))$ complexity in bit operations. Even then, unranking for all $N$ codebook entries would raise the overall time complexity from $O(d \cdot N)$ to $O(d^2 \cdot \log_2(d) \cdot N)$, clearly violating the second constraint.

However, partial sorting can be used to drastically cut down the overall number of operations. In practice, $N$ is extremely large - applications to very large databases is indeed a key motivation of hashing. In comparison the number $K$ of top items to retrieve should be negligible, especially under real-time circumstances.

It is therefore safe to assume we can find $K'$ such that $K \gg K' \gg K$. Using partial sorting, $N - K'$ irrelevant items can then be filtered out based on the raw Hamming distance, without accounting for uncertainty. This costs the same $d \cdot N$ XOR operations as previously. Within the remaining $K'$ items, using uncertainty only requires an additional $O(d^2 \cdot K')$, which can be considered small next to $d \cdot N$.

The overall encoding and retrieval pipeline for ULA-CODE, including the use of compressed uncertainty, is shown in Figure 10.

3.7. Encoder training & codebook preparation & evaluation

Hashes of size 96, 128, 192, 256 are employed. The same model trained on the 81000 clips from the training set is evaluated across the three test sets described in Section 3.2 to assert the versatility of the retrieval system. As stated in Section 3.4 we first train SSTH-RT+ as the primary for LA-CODE. This time, the secondary is trained for a maximum of 30 epochs.
with early stopping based on bitwise accuracy measured on the validation set. Batch size is set to 86; the learning rate is $1e^{-3}$.

ULA-CODE reuses LA-CODE's pair of encoders; the difference is in the way the codebook is built, since we incorporate the uncertainty defined above. ULA-CODE's fairly narrow hyperparameter space is explored with all 80 combinations shown in Figure 9.

Testing follows the same protocol found in Yu and Padoy (2020), by separating the test set in two according to the splits established in Section 3.2. Videos in the first part serve as queries while the second part plays the role of the database to search into, or codebook.

As usually done in video retrieval evaluation (Zhang et al. 2016), we report the Mean Average Precision in the top K search results (mAP@K), with mAP@10 as the main reference. Even though we use clips of uniform duration, the incremental nature of our methods enable efficient retrieval in real time, at any point inside the clip; a possibility that was not offered in other video hashing studies (Zhang et al. 2016; Song et al. 2018; Wu et al. 2017; Liu et al. 2019). By doing so during testing, we essentially try to examine the retrieval system’s dynamic behavior in response to the context; after watching only a portion of a clip, can the system quickly return relevant videos? We therefore report mAP@10 for one third and two thirds of a clip, in addition to the entirety of the clip (roughly 10, 20 and 30s respectively).

### 4. Results

| Bypass40 | Cholec80 | CEV64 |
|----------|----------|-------|
| $\gamma$, $\theta$, $K_{bs}$ | $\gamma$, $\theta$, $K_{bs}$ | $\gamma$, $\theta$, $K_{bs}$ |
| 64 | 1 | 0 | 24 | 1 | 0.5 | 16 | 0.75 | 0 | 24 |
| 96 | 1 | 0 | 24 | 0.5 | 0 | 36 | 0.75 | 0.25 | 36 |
| 128 | 0.75 | 0 | 48 | 0.75 | 0.25 | 64 | 0.75 | 0 | 48 |
| 192 | 0.75 | 0.5 | 48 | 0.5 | 0.25 | 72 | 0.75 | 0 | 96 |
| 256 | 1 | 0 | 64 | 1 | 0 | 96 | 1 | 0 | 64 |
| 384 | 0.75 | 0.25 | 144 | 0.5 | 0.25 | 96 | 0.75 | 0.25 | 144 |

Table 2. ULA-CODE optimal parameter combinations for each bitrate size and test protocol.

### 4.1. Main comparison against baselines

We start with a global comparison of ULA-CODE against the baseline methods, SSTH-RT$^+$ and LA-CODE. mAP@10 results are displayed in Figure 11. Since ULA-CODE depends on hyperparameters $\gamma$, $\theta$, $K_{bs}$, we provide two ways of observing its performance. Results for max ULA-CODE show the method at its best, with an optimized set of hyperparameter values shown in Table 2. Results for avg ULA-CODE, on the other hand, show the average performance over the entire hyperparameter space. mAP@10 is plotted with levels of observation on the x-axis, at 10s, 20s and the end of the clip. All hash sizes are shown, one in each row.

Results for avg ULA-CODE surpass our previous approach LA-CODE by 1 to 2%. This means, even with a random choice of $\gamma$, $\theta$, $K_{bs}$, ULA-CODE improves performance on average. An optimized choice of parameters doubles those gains, beating LA-CODE by a 3 to 4% margin. The performance order between the approaches is mostly consistent - best ULA-CODE, followed by average ULA-CODE, then LA-CODE and finally SSTH-RT$^+$. For surgical events, across all hash sizes and levels of observation, avg ULA-CODE exceeds the baseline LA-CODE by a mostly consistent 2% margin. Globally, performance is slightly higher for Cholec80 (especially for 128 and 192 bits), possibly due to a simpler workflow than Bypass40, and visually simpler content than CEV64.

Interestingly, performance does not necessarily increase with the observation level $\alpha$. This could be due to the fact that the end of video clips can sometimes be close to a surgical phase or critical event boundary, where discriminative information disappears and more ambiguous information can be present; for Cholec80 this is particularly noticeable.

Overall, mAP@10 retrieval results for surgery are roughly on par with results shown on generic activities (Yu and Padoy 2020), which suggests video retrieval is viable in the surgical domain as well. Along with this statement, it is important to keep in mind the key differences between surgical data and generic data: on the one hand, the higher number of classes (≈ 200) in generic video datasets such as FCVID (Jiang et al. 2018) or ActivityNet (Heilbron et al. 2015) adds to the difficulty of the problem. On the other hand, surgery videos are much harder to interpret: visual cues for a phase or an event can be sparse, if not misleading - as evidenced in the qualitative results shown later (Section 4.3). Context also plays an important role; by using all the frames from the beginning of the surgery, Twinanda et al. (2016b); Jin et al. (2018); Czempiel et al. (2020); Ramesh et al. (2021) were able to achieve state-of-the-art surgical phase recognition results. Short clips are an appropriate format for retrieval in real time due to the fast pace of this task, but they inevitably miss the overarching workflow they are a part of.

### 4.2. Influence of hyperparameters

We then examine each of the three hyperparameters in ULA-CODE separately, to understand how they affect retrieval performance. Results are plotted in Figure 12. Here max ULA-CODE is obtained by fixing the value of one hyperparameter, then taking the maximum over hyperparameter combinations featuring that value. Similarly, avg ULA-CODE is...
now defined by fixing a hyperparameter’s value averaging over all corresponding combinations. LA-CODE without any uncertainty sets our baseline. Results for 256 bits are displayed in Figure 12. In this figure, a performance data point is obtained for every:

- protocol (Bypass40, Cholec80, CEV64) - plot grid column
- hyperparameter value - x-axis
- observation level $\alpha$ - line color
- approach type (LA-CODE, avg ULA-CODE or max ULA-CODE) - line texture

Results for other hash sizes (64, 96, 128, 192, 384) are shown in the supplementary material, section B.

Across all hyperparameters, max ULA-CODE is obviously superior to avg ULA-CODE, which is itself in most cases above LA-CODE. For 256 bits on Bypass40 at full observation, LA-CODE achieves 38%, which is beaten by avg ULA-CODE with a 1.2% minimum margin, and by max ULA-CODE by 2 to 3%. For the same code size and observation level on Cholec80, LA-CODE sets the baseline at 39%, again surpassed by avg ULA-CODE (41.5%) and max ULA-CODE (41.3 to 42%). Similar observations can be made for surgical events with LA-CODE at 38.8%, avg ULA-CODE ranging from 39.5 to 41% and max ULA-CODE ranging from 40.2% to 42.2%.

For the $\gamma$ parameter (Figure 12), we can see a slight trend favoring higher values: for instance, for 256 bits on surgical events at 2/3 observation, max ULA-CODE goes from 41.2% at $\gamma = 0$ to 41.5% at $\gamma = 1$. In general, this suggests stricter suppression of uncertain bits improves retrieval performance.

For $\theta$, it appears that lower values generally lead to higher mAP@10; such as for surgical events with 256 bits at 2/3 observation, the dropoff from $\theta = 0$ to $\theta = 1$ is over 2%. We can therefore assume that Type II uncertainty is in general more informative, and has higher odds of pointing towards faulty bits in the hash. Retrieval is performed by matching a code from the secondary with codes from the primary, giving a possible explanation as to why Type II is a slightly better uncertainty measurement.

The trend for $K_{bs}$ is more subtle: results slightly lean towards higher values. This trend implies the number of untrustworthy bits is generally close to half the size of the hash, introducing a slight downside: the compressibility of the uncertainty pattern decreases as the number of uncertain bits to report gets close to $d/2$.

For every code size and protocol, we are able to obtain an optimal value based on the highest mAP@10 achieved by ULA-CODE, averaged over all levels of observation. These are the optimal hyperparameters are reported in Table 2. The combinations found seem to confirm the trends observed: higher values of $\gamma$ and $K_{bs}$, lower values for $\theta$.

4.3. Additional results

While retrieval mAP can be relied upon for quantitative evaluation, the in-depth behavior of our method can be dif-
Fig. 11. Mean average precision over different levels of observation $\alpha$, for all three datasets (columns) and all six hash sizes (rows). For avg ULA-CODE, error bars accounting for one standard deviation around the mean are displayed.
Fig. 12. Influence of hyperparameters on ULA-CODE’s performance: uncertain bit suppression rate \( \gamma \) (first row), primary-secondary balance \( \theta \) (second row), number of uncertain bits \( K_{bs} \) (third row). Results are shown for 256-bit hashes, on all three test sets (columns). For mean ULA-CODE, error bars accounting for one standard deviation around the mean are displayed.
Fig. 13. Qualitative results on CEV64, with and without using uncertainty. Each row shows a query (left) and the top 5 search results from LA-CODE (top) and ULA-CODE. Red indicates an incorrect video, green a correct one. Top left of the thumbnail: raw Hamming distance, used by LA-CODE. Top right of the thumbnail: Hamming distance modulated by uncertainty, used by ULA-CODE. The hash is on the right side of each thumbnail, with uncertain bits in purple.
difficult to grasp based on these measurements only. To provide more insight, we first present a per-class breakdown of retrieval results for ULA-CODE in the supplementary material. Section D. We also provide qualitative results in Figure 13 for surgical video retrieval, comparing search results returned by LA-CODE and ULA-CODE. Three clips are used as queries, taken from the CEV64 dataset: mesh placement, dividing and incising. Green indicates an event correctly matching with the query; red, an incorrect search result. We display the hash corresponding to a video next to its thumbnail: white is a 0, black a 1. In hashes for the top 5 search results, uncertain bits appear in purple: clear for an uncertain 0, dark for an uncertain 1. The raw Hamming distance to the query, used by pear in purple: clear for an uncertain 0, dark for an uncertain 1. In hashes for the top 5 search results, uncertain bits appear in purple: clear for an uncertain 0, dark for an uncertain 1. The raw Hamming distance to the query, used by LA-CODE, is shown at the top left of the thumbnail; while the Hamming distance modulated by uncertainty used by ULA-CODE is shown at the top right. The code size used is 128; for ULA-CODE, the parameters used are $\gamma = 0.75$, $\theta = 0$, $K_0 = 64$.

The purple bits, marked as uncertain according to our method, do turn out to be misleading: due to them, LA-CODE returns several irrelevant results - e.g. in the second row, bleeding instead of dividing. By ignoring them, ULA-CODE is able to find two more correct videos. In the last row, LA-CODE’s top result (background) is pushed down by ULA-CODE to number 4; LA-CODE’s fourth best (abdominal access) exits ULA-CODE’s top 5.

More importantly, those queries exemplify the difficulty of video retrieval in surgery; search results marked as incorrect are often understandable, and make sense visually to some extent. During body exits, the laparoscope is placed on a cloth that resembles the mesh employed in abdominal wall procedures, hence the confusion in the first row. Bleeding inevitably occurs during tissue division; in the second row this introduces ambiguity with CEV64’s actual bleeding event, defined as active bleeding. Even abdominal access in the third row features a trocar resembling the shaft of an instrument.

For more dynamic and in-depth qualitative results, a video with side-by-side comparisons of LA-CODE and ULA-CODE is provided in the supplementary material. Note that this video is rendered offline, with videos retrieved instantly as soon as the hash is regenerated; real-time inference would add some amount of latency. Using our setup (Intel i7-6800k CPU, NVIDIA 1080 Ti GPU), elements from the entire inference pipeline (I3D feature extraction, hash generation, search with uncertainty) altogether do not exceed 1s of inference time.

4.4. Discussion & future work

As evidenced by the qualitative results, evaluation of video retrieval systems - not only in surgery, but in general - is a challenging open problem. One important path to explore in future work would be to design quantitative evaluation protocols that better capture the usability of the system than the current one based on retrieval mAP. While, on average, our method solidly outperforms baselines that do not factor in uncertainty, more expressive means of evaluation would enable looking into possible failure cases (e.g. events in the video having their contribution to the hash wrongly decreased). Performance-wise, a few possibilities may be considered for future improvements: the current method being completely unsupervised, mixing in some form of human-labeled supervision (surgical phase, actions, instruments for example) is likely to enhance retrieval - this of course introduces a tradeoff between performance and cost of annotations, and might affect generalizability by favoring a particular set of labels. New work on self-supervised learning also hints at interesting possibilities. The current visual backbone is pretrained on Kinetics; self-supervised pretraining on surgical videos might result in increased performance by making the backbone more domain-specific, without requiring manual labels.

Conclusion

This work targets the task of live video-to-video retrieval on diverse, large-scale surgical video data. We perform live surgical video retrieval with the LA-CODE method on datasets of recorded surgeries. Additionally, we expose and address the problem of uncertain bits used in the codebook by measuring their degree of uncertainty, then reporting it in the codebook in a highly compressed manner. This awareness of uncertain bits is the core of our proposed ULA-CODE method, which provides up to 4 % improvement in terms of retrieval mAP@10, measured using three semantic contexts in surgery: phases for cholecystectomy, phases for bypass and surgical events, introduced for the first time in our work. Usability on this wide range of semantics, across many types of workflows and procedures is promising in terms of generalizability for our method.

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Ethical approval

The surgical videos were recorded and anonymized following the informed consent of patients in compliance with the local Institutional Review Board (IRB) requirements.

Patient consent

The patients consented to data recording.

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