Exploring strategies for classification of external stimuli using statistical features of the plant electrical response

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Plants sense their environment by producing electrical signals which in essence represent changes in underlying physiological processes. These electrical signals, when monitored, show both stochastic and deterministic dynamics. In this paper, we compute 11 statistical features from the raw non-stationary plant electrical signal time series to classify the stimulus applied (causing the electrical signal). By using different discriminant analysis-based classification techniques, we successfully establish that there is enough information in the raw electrical signal to classify the stimuli. In the process, we also propose two standard features which consistently give good classification results for three types of stimuli—sodium chloride (NaCl), sulphuric acid (H2SO4) and ozone (O3). This may facilitate reduction in the complexity involved in computing all the features for online classification of similar external stimuli in future.

1. Introduction

Plants produce electrical signals, when subjected to various environmental stimuli [1–7]. These electrical signals in essence represent changes in underlying physiological processes influenced by the external stimuli. Thus, analysing such plant electrical signals may uncover possible signatures of the external stimuli embedded within the signal. The stimuli may vary from different light conditions, burning, cutting, wounding, gas or liquid [8], etc. This opens up the possibility to use such analysis techniques to turn a green plant into a multiple-stimuli sensing biological sensor device [9]. If such an association between the external stimuli and the resulting plant electrical signal could be made, then it may serve the purpose of holistic monitoring of environmental constituents at a much cheaper cost (because of abundance of plants), thereby eliminating the need to install multiple individual sensors to monitor the same external stimuli. In this work, we attempt to explore the possibility of classifying three external stimuli—sodium chloride (NaCl), sulphuric acid (H2SO4) and ozone (O3)—from the electrical signal response of plants as the first step towards that goal. Here, we chose heterogeneous stimuli that reproduce some of the possible environmental pollutants, e.g. H2SO4 is a major component of acid rain. Ozone is a tropospheric air pollutant and is the main component of smog. Salinization often results from irrigation management practices or treatment of roads with salt as the de-icing agent and can be linked to environmental soil pollution. These three stimuli—NaCl, H2SO4, O3—are specifically chosen to study the change in plant physiological response to represent the effect of environmental pollution.

Electrical signals were collected from a number of tomato (Solanum lycopersicum) and cucumber (Cucumis sativus) plants using NaCl, H2SO4 and O3 as stimuli in controlled settings. Multiple experiments were conducted for each stimulus to ensure the repeatability of the electrical signal response each time. We then
extracted 11 statistical features from these plant signal time series in order to investigate the possibility of accurate detection of the external stimulus through a combination of these features and simple discriminant analysis classifiers. We believe this work will not form the backbone of using plants as environmental biosensors [9,10] but also open up a new field of further exploration in plant signal behaviours with meaningful feature extraction and classification similar to the studies done using other human body electrical responses such as electrocardiogram (ECG), electroencephalogram (EEG) and electromyogram (EMG) [11]. Although there have been few recent attempts on signal processing, feature extraction and statistical analysis using plant electrical responses [12–18], there has been no attempt to associate features extracted from plant electrical signals to different external stimuli. The focus of our work is to address this gap. Here, we analysed the statistical behaviour of raw electrical signals from plants similar to previous studies on raw non-stationary biological signals which exhibit random fluctuations such as EMG/EEG, adopting a similar approach to develop a classification system [19–22]. The present paper reports the first exploration of its kind, aiming at finding meaningful statistical feature(s) from segmented plant electrical signals which may contain some signature of the stimulus hidden in them, to different extents.

As a first exploration, this work focused on the ability to classify the stimuli by only looking at a small segment of raw plant electrical responses. The questions that arise in order to explore this possibility of classification are: (i) which features give a good discrimination between the stimuli and (ii) which type of simple classifier will give a consistently good result? The simplicity of the classifier is an important issue here because our ambition is to run it on resource-constrained embedded systems, such as sensor nodes in future. In order to tackle the first question, we start by using 11 statistical features that have been used in other biological signals (e.g. EEG, ECG and EMG) [11]. We here explore which feature alone (univariate analysis) or feature combinations (bivariate analysis) consistently indicate towards that particular signature of the stimulus. In order to answer the second question, we will start with a simple discriminant analysis classifier and then its other variants to observe the average classification rate.

### 2. Material and methods

#### 2.1. Stimulus and experimental details

Here we try to develop a classification strategy to detect three different stimuli viz. O₃, H₂SO₄, NaCl. Four sets of experiments were conducted with H₂SO₄, NaCl 5 ml and 10 ml each as stimuli, as shown in Table 1. For each stimuli mentioned above, a between-subjects design for experiments was set up where four different tomato plants (similar age, growing conditions and heights) were used with each plant being exposed to the stimulus only once. Thus, for 12 experiments, 12 tomato plants were used. For ozone as the stimulus, six cucumber plants and two tomato plants were used for eight experiments with each plant being subjected to only one experiment but multiple applications of the stimulus.

For each plant, we used three stainless steel needle electrodes—one at the base (reference for background noise subtraction), one in the middle and the other on top of the stem as shown in figure 1. The electrodes were 0.35 mm in diameter and 15 mm in length, similar to those used in EMG from Bienen S.A.S. and were inserted around 5–7 mm into the plant stem so that the sensitive active part of the electrodes (2 mm) were in contact with the plant cells [8]. The electrodes were connected to the amplifier–data Acquisition (DAQ) system in a same way as in [8]. Plants were then enclosed in a plastic transparent box with openings to allow the presence of cables and inlet/outlet tubes, and exposed to artificial light conditions (LED lights responding to the plant’s photosynthetic needs, mimicking a day/night cycle of 12 h). Each experiment was conducted in a dark room to avoid external light interferences. The whole setup was then placed inside a Faraday cage to limit the effect of electromagnetic interference as shown in figure 1.

After the insertion of the electrodes into the plant, we waited for approximately 45 min to allow the plant(s) to recover before starting the stimulations. Electrical signals acquired by the electrodes were provided as input to a two-channel high impedance (10¹⁵ Ω) electrometer (DUO 773, WPI, USA) while data recording was carried out through four-channel DAQ (LabTrax, WPI) and its dedicated software LABSCRIBE (WPI; http://www.wpiinc.com/blog/2013/05/01/product-information/data-trax-software-for-labscribe/). The sampling frequency was set as 10 samples s⁻¹ for all the recordings. For the treatments with liquid, sulfuric acid (5 ml H₂SO₄, 0.05 M) or sodium chloride (5 or 10 ml NaCl 3M), a syringe placed outside of the Faraday cage and connected to a silicone tube inserted into the plant soil, was used to inject the solution as shown in figure 2a. O₃, produced by a commercial ozone generator (mod. STERIL, OZONIS, Italy; http://www.sepra.it/products-linea-generatiori-serie-stel20mng03h-da-aria-6.html) was injected into the box through a silicone tube (1 mm spray every 2 h, 16 ppm), while a second outlet tube threw the ozone from the box to the chemical hood as shown in figure 2b. The concentration of ozone inside the box was monitored using a suitable sensor.

#### 2.2. Data processing and segmentation

Each dataset was obtained after one (H₂SO₄, NaCl 5 ml and 10 ml) or multiple (O₃) applications of that particular stimulus. This is illustrated in figure 3 where the application of stimulus is marked by a vertical dotted line with the post-stimulus part of the time series on the right side and the background or pre-stimulus part indicated on the left side of the line. In the

| stimulus           | plant species used | concentration and application                          | no. data points |
|--------------------|--------------------|---------------------------------------------------------|-----------------|
| ozone (O₃)         | tomato/cucumber    | 16 ppm for a minute, every 2 h                          | 1881            |
| sulfuric acid (H₂SO₄) | tomato          | 5 ml of 0.05 mol H₂SO₄ in the soil once                  | 496             |
| sodium chloride (NaCl)—5 ml | tomato  | 5 ml of 3 mol NaCl solution in the soil once           | 812             |
| sodium chloride (NaCl)—10 ml | tomato | 10 ml of 3 mol NaCl solution in the soil once         | 612             |

Table 1. Different stimulus, plants species and number of data points (each capturing 11 statistical measures of 1000 samples) used for the present study.
As a general observation, from figure 3 we can see that there are sudden spiking changes in the signal after the application of H₂SO₄ and ozone as stimulus. However, for the NaCl 5 ml and 10 ml stimuli, the changes in the electrical signal response are relatively slow. Thereafter, for each experiment, we divided the data such that we have a post-stimulus part of the signal as well as the background (pre-stimulus) part. In the case of O₃ where multiple stimuli were applied, we divided the data such that the signal duration between consecutive applications of the stimuli was a separate post-stimulus response. This way, we ended up having several post- and pre-stimuli datasets for all four stimuli. Next, each of these datasets was segmented into blocks of fixed window length of 1000 samples (100 s) which is shown in figure 3.

The reason for this data segmentation is to facilitate batch processing of large volumes of data acquired during continuous monitoring. We extracted 11 statistical features from these small chunks of 1000 samples and wanted to explore whether the features from such small chunks give enough information to the classifier to discriminate which stimulus that particular data chunk (time period) belonged to. Again, a successful classification of the stimulus from the features of such a small signal block will enable a fast decision time. This is due to smaller buffer-size for batch processing compared to the whole length of the signal acquisition thereby making it easier for possible online implementation in future. As this is the first exploration of its kind, we confine the study to 1000 samples only, for extracting statistical features that provide sufficiently good classification accuracy but there is scope for further exploration of an optimum window length to classify the stimulus. The classifier was trained using only the blocks of samples belonging to the post-stimulus part of the plant signal. The pre-stimulus part was also divided into similar segments in order to study the effect of the background for different plants under different experimental conditions.

The stimulus-induced plant signals have both deterministic and random dynamics, i.e. local and global variations in amplitudes and different statistical measures of smaller data segments [6,9,10,23,24]. The research question that we attempted to answer through the present exploration is—is it possible to identify the stimulus by only looking at the statistical behaviour of small segments of the plant’s electrical response? A successful answer to this question would pave the way for conceptualizing an electronic sensor module in the future for classifying the
environmental stimulus. This sensor module can be fitted on the
plant for batch processing of segmented plant signals, statistical
feature extraction and classification, without much memory
requirement in future applications.

2.3. Statistical feature extraction from segmented time
series
Here, we started with 11 features that are predominantly used in
the analysis of other biological signals [25]. Different descriptive
statistical features like mean ($\mu$), variance ($\sigma^2$), skewness ($\gamma$), kur-
tosis ($\beta$) as given in (2.1) and interquartile range ($\text{IQR} = Q_3 - Q_1$),
i.e. the difference between the first and third quartile) were
calculated as

$$\mu = E[x_i], \quad \sigma^2 = E[(x_i - \mu)^2], \quad \gamma = E[(x_i - \mu)^3]/\sigma$$

and $\beta = E[(x_i - \mu)^4]/\sigma^4$. (2.1)

In the calculation of four basic moments in (2.1), $x_i$ is the seg-
mented raw electrical signals each of them containing 1000
samples and $E[\cdot]$ is the mathematical expectation operator.
Apart from these five, the remaining six features taken are:
Hjorth mobility, Hjorth complexity, detrended fluctuation
analysis (DFA), Hurst exponent, wavelet packet entropy and
average spectral power which are briefly described below.

2.3.1. Hjorth’s parameters
The Hjorth mobility and complexity, described in [26], quantify a
signal from its mean slope and curvature by using the variances of
the deflection of the curve and the variances of their first and
second derivatives. Let the signal amplitudes at discrete time instants
be $x_n$ at time $t_n$. The measures of the complexity of the signal is based
on the second moments in the time domain of the signal and the sig-
nal’s first and second derivatives. The finite differences of the signal
or time derivatives can be viewed as follows:

$$d_n = d_{n+1} = a_{n+1} - a_n, \quad \text{where } n = 1, 2, \ldots, (N-1)$$

and $d_n = d_{n+1} = a_{n+1} - a_n, \quad \text{where } n = 1, 2, \ldots, (N-2)$. (2.2)

The variances are then computed as [27]

$$\sigma_d^2 = \frac{1}{N} \sum_{n=1}^{N} (d_n)^2, \quad \sigma_{dd}^2 = \frac{1}{(N-1)} \sum_{n=1}^{N-1} (d_n - d_{n-1})^2$$

and $\sigma_{dd}^2 = \frac{1}{(N-2)} \sum_{n=1}^{N-2} (d_n - d_{n-1})^2$. (2.3)
These variances (2.3) are used to calculate the Hjorth mobility (m₁) and the Hjorth complexity (c₁) [27] as
\[ m₁ = \frac{\sigma_d^2}{\sigma_a^2} \quad \text{and} \quad c₁ = \frac{\sqrt{\left(\frac{\sigma_d^2}{\sigma_a^2}\right)^2 - \left(\frac{\sigma_s^2}{\sigma_a^2}\right)^2}}{\sigma_a^2}, \] (2.4)

2.3.2. Detrended fluctuation analysis
The DFA has been introduced in identifying long-range correlations in non-stationary time-series data. By using a scaling exponent (a), one can describe the significant autocorrelation properties of signals also with a provision of capturing the non-stationary behaviour [28,29]. The different values of a represent certain autocorrelation properties of the signal [28,29]. For a value of less than 0.5, the signal is described as anti-correlated. A value of exactly 0.5 indicates uncorrelated (white noise) signal, whereas a value greater than 0.5 indicates positive autocorrelation in the signal. When a = 1, the signal is indicated to be 1/f noise and a value of 1.5 indicates the signal to be random walk or Brownian noise [28,29].

2.3.3. Hurst exponent
The Hurst exponent (H), a dimensionless estimator similar to DFA, is used as a measure of the long-term memory of a time-series data x_l [30,31]. The value of the Hurst exponent lies between 0 and 1, with a value between 0 and 0.5 indicating anti-persistent behaviour. This denotes that a decrease in the value of an element will be followed by an increase and vice versa. This characteristic is also known as mean reversion, which is explained as the tendency of future values to return to longer term mean values. The mean reversion phenomenon gets stronger for a series with an exponent value closer to zero [30,31]. When the value is close to 0.5, a random walk (e.g. a Brownian time series) is indicated. In such a time series, there is no correlation between any element and predictability of future elements is difficult [30,31]. Lastly, when the value of the exponent is between 0.5 and 1, the time series exhibits persistent behaviour. This means the series has a trend or there is a significant autocorrelation in the signal. The more closer the exponent value gets towards unity, a stronger trend is indicated for the time series [30,31].

2.3.4. Wavelet entropy (wentropy)
The time series may be represented in frequency and/or time-frequency domains by decomposing the signal in terms of basis functions such as harmonic functions (as in Fourier analysis) or wavelet basis functions (with consideration of non-stationary behaviour), respectively. Given such decomposition, it is possible to consider the distribution of the expansion coefficients on this basis. Quantification of the degree of variability of the signal could be done using the entropy measure, where high values indicate less ordered distributions. The wavelet packet transform based entropy (WE) measures the degree of disorder (or order) in a signal [32–34]. A very ordered underlying process of a dynamical system may be visualized as a periodic single frequency signal (with a narrow band spectrum). Now the wavelet transformation of such a signal, will be resolved in one unique level with a value nearing one, and all other relative wavelet energies being minimal (almost equal to zero) [32–34].

On the other hand, a disordered system represented by a random signal will portray significant wavelet energies from all frequency bands. The wavelet (Shannon) entropy gives an estimate of the measure of information of the probability distributions. This is calculated by converting the squared absolute values of the wavelet coefficients s_i of the i-th wavelet decomposition level as
\[ WE = -\sum_i s_i \log (s_i^2). \] (2.5)

2.3.5. Average spectral power
The average spectral power (P) is the measure of the variance of signal power, distributed across various frequencies [35]. It is given by the integral of the power spectral density (PSD) curve \( |X(e^{i\omega})|^2 \) of the signal x(t) within a chosen frequency band of interest (bounded by the low and high frequency—\( \omega_l \), \( \omega_h \), respectively) as
\[ P = \int_{\omega_l}^{\omega_h} |X(e^{i\omega})|^2 \, d\omega. \] (2.6)

2.4. Adopted classification scheme
All of the above-mentioned extracted features are first normalized to scale them within a maximum (1) and minimum (0) value and to avoid any unnecessary emphasis of some of the features on the classifier weights owing to their larger magnitude than the others. Among all the 11 features, their relative importance in each of the binary classification set has been obtained by computing the Fisher’s discriminant ratio (FDR) [36]. The FDR is a measure to explore the discriminating power of a particular feature to separate two classes and are computed as \( (\mu_1 - \mu_2)^2/(\sigma_1^2 + \sigma_2^2) \) [36], where, \( \mu_1 \) and \( \mu_2 \) are the mean and \( \sigma_1 \) and \( \sigma_2 \) are the standard deviation of the features in the two classes, respectively, and therefore should not be confused with that of the raw signal in (2.1). Higher ranking, based on FDR, will be assigned to those features that have higher difference in the mean values and small standard deviation implying compact distinctly located clusters. Owing to the application of multiple-stimulus, the FDR-based feature ranking is applied for each of the stimulus pairs, in this work [36].

The classifiers implement algorithms which help in distinguishing between two or more different groups or classes of data. Different classification algorithms are obtained by first training the class labels (stimulus applied in this case) of a certain portion of the known (training) groups and then using the trained model to predict the class labels for a group of unknown (test) dataset. Once it is found that the testing phase is successful (high accuracy in identifying the stimulus) using the trained model, the algorithm can be used to identify which class unknown data belongs to. In cases, where the distinction is easily achievable, discriminant analysis classifiers such as linear discriminant analysis (LDA) could be effective. Where such distinctions are not that straightforward, nonlinear classifiers such as kernel-based techniques such as support vector machine (SVM) can be applied. Cases where only two groups need to be identified, binary classification are generally carried out. This is a much simpler process than multiple class classification. The choice of a classifier (discriminant or complex kernelized SVM) may be determined sometimes by looking at the distribution plot of the features of the two groups. If the distribution plots show two well-separated means, we can conclude that a simple linear or other discriminant analysis-based classifiers should be able to classify the data to a sufficient extent. Unnecessarily involving a complex nonlinear classification technique often gives high classification accuracy on the training dataset, but is prone to over-fitting. In this study, we focus on five different discriminant analysis classifiers which are based on least square method for training the classifier weights rather than the computationally heavy optimization process involved in SVM. Among five discriminant analysis variants, the QDA uses a quadratic kernel with the feature vectors. The Diaglinear and Diagquadratic classifiers are also known as naive Bayes classifier using a simple linear and quadratic kernel and use the diagonal estimate of the covariance matrix (neglecting the cross-terms or feature correlations). The Mahalanobis classifier uses a different distance measure than the standard Euclidean distance [36]. We used different discriminant analysis classifiers owing to their simplicity to see the characteristic changes.
traced in the features owing to these stimuli. Two types of approach could be taken in classification (i) choice of meaningful statistical features followed by simple classifier and (ii) simple features followed by a complex classifier. The former case is preferable to the latter as it may help in understanding the change in statistical behaviour of the signal which might be indicative towards some consistent modification of the underlying biological process.

Cross-validation schemes are often used to avoid the introduction of any possible bias owing to the training dataset [36]. Here we use the leave one out cross validation (LOOCV) where, if there are N data points, then (N − 1) number of samples are used for training the classifier and the one held-out sample is used to test the trained structure. Thereafter, the single test sample will be included in the next training set, and again a new sample from the previous training set will be set aside as the new test data. This loop will go for N times, until all the samples have been tested and the average classification accuracy for all the N instances are calculated [36].

3. Results

The classification results of five discriminant analysis classifier variants, using 11 statistical features from plant electrical signal response to four different stimuli viz. H$_2$SO$_4$, NaCl of 5 ml and 10 ml and O$_3$ are presented in this section. We also investigate which stimuli are best detected by looking at the classification accuracy, thereby suggesting the ability of the plant to detect few particular stimuli better than the others.

3.1. Need for subtracting the background information of individual features

Figure 3 shows the four plant electrical signal responses to four different stimuli beginning at different amplitude levels. This means the background signal (even before the application of the stimuli) is different in all four different cases. This may bias the final classification result owing to the already separated background information within the multiple features considered. Owing to the effect of different backgrounds, we can see a clear separation between the stimuli for some features such as Hjorth mobility, Hjorth complexity and skewness, in figure 4, where histogram plots for each of the features for each stimulus are plotted without any background subtraction.

This encourages us to look at only the incremental values of the features under different stimuli. The incremental values are obtained by subtracting the mean of every feature extracted from the background from the corresponding feature extracted from the post-stimulus part of the signal. The histogram plots of the incremental values of the individual features, after the background is subtracted, are given in figure 5 which shows a lesser separability in the stimuli which were as expected. We now use these incremental values of the features to see how good they are in providing a successful classification (using five different discriminant analysis classifier variants) between any two stimuli (six binary combinations of four stimuli). As an example, although the histogram plots in figure 5 shows clear separation of the distributions for NaCl and O$_3$ using skewness as feature owing to their peaky nature, the frequency of occurrence of the histograms show that the distributions have wider spread which has been reflected by the moderate rate of classification reported in the next subsections using that particular feature.

3.2. Correlation of features to avoid redundancy

Between all the features, a correlation test was carried out to find out their inter-dependence. The result of this test,
given in Table 2, is obtained by checking the Pearson correlation coefficient values between all feature pairs. A correlation value of (approx. ±1) indicates a strong positive/negative correlation between a pair, whereas a value closer to zero indicates the feature pairs are independent and are thus more informative about the underlying process. A good classification strategy should ideally involve uncorrelated features, in order to avoid redundancy in training the classifier. In this work, we proceeded by initially taking all features into account and then ignored the ones with high correlation.

### 3.3. Classification using univariate and bivariate features

The classification results were obtained in two ways—using univariate and bivariate features, to make the analysis intuitive and simple to infer. That is, instead of taking all the features together to get a multivariate classification (which may give good classification accuracy but are less intuitive and reliable owing to increases in complexity and dimension of the problem), we just explored the results with 11 individual features and 55 possible feature pairs.

Table 3 presents the results, obtained using individual features, averaged across all six stimuli combinations and all five different classifier variants. We have also presented the relative multi-class separability score given by the scatter matrix (S) in (3.1) for each feature in terms of the within-class ($S_w$) and between-class ($S_b$) scatter matrix [36].

$$S = \text{trace}(S_w^{-1} S_b)$$

and

$$S_w = \sum_{i=1}^{c} P_i S_i, \quad S_b = \sum_{i=1}^{c} P_i (\mu_i - \mu_{0}) (\mu_i - \mu_{0})^T,$$

where $P_i$ is the a priori probability for the present four-class problem ($c = 4$) and has been considered as 1/4. Also, the

### Table 2. Correlation coefficient between 11 statistical features extracted from plant electrical signals (after subtracting the mean of the pre-stimulus features from the post-stimulus ones).

| features     | $\mu$ | $\sigma^2$ | IQR  | $\gamma$ | $\beta$ | $m_a$ | $c_b$ | $H$ | $\alpha$ | WE | $p$ |
|--------------|-------|------------|------|----------|---------|-------|-------|-----|----------|----|-----|
| $f_1 = \mu$  | 1.00  | 0.09       | -0.03| -0.06    | 0.07    | 0.04  | 0.03  | -0.11| -0.22    | 0.70| 0.26 |
| $f_2 = \sigma^2$ | *     | 1.00       | 0.83 | 0.01     | 0.10   | -0.05| -0.23| -0.10| 0.21     | 0.02| 0.07 |
| $f_3 = \text{IQR}$ | *     | *          | 1.00 | 0.04     | -0.08 | 0.31 | 0.01  | 0.53 | -0.12    | 0.05|      |
| $f_4 = \gamma$ | *     | *          | 1.00 | 0.29     | 0.00  | -0.06| -0.09| -0.07| -0.08    | 0.00|      |
| $f_5 = \beta$  | *     | *          | *    | 1.00     | -0.01| -0.23| -0.14| -0.03| 0.14     | 0.06|      |
| $f_6 = m_a$    | *     | *          | *    | *        | 1.00  | 0.34 | -0.07| -0.10| 0.06     | 0.02|      |
| $f_7 = c_b$    | *     | *          | *    | *        | 1.00  | 0.12 | -0.28| 0.06 | 0.09     |     |      |
| $f_8 = H$      | *     | *          | *    | *        | *     | 1.00 | 0.64 | -0.15| -0.16    |     |      |
| $f_9 = \alpha$ | *     | *          | *    | *        | *     | *   | 1.00 | -0.29| -0.06    |     |      |
| $f_{10} = \text{WE}$ | * | * | * | * | * | * | * | * | 1.00 | -0.09 |      |
| $f_{11} = P$   | *     | *          | *    | *        | *     | *   | *    | *   | 1.00     |     |      |

### Table 3. Average accuracy (averaged across all six binary stimuli combinations and all five classifier variants) and best accuracy (averaged across four ‘one versus rest’ stimuli combinations) for classification using individual features.

| ranked features     | scatter matrix | average accuracy for all binary stimulus combinations (%) | best accuracy for all ‘one versus rest’ stimulus combinations (%) |
|---------------------|----------------|----------------------------------------------------------|------------------------------------------------------------------|
| $F_1$ mean ($\mu$)  | 0.8453         | 70.87                                                    | 73.01, Mahalanobis                                               |
| $F_2$ wentropy (WE) | 0.2858         | 69.79                                                    | 62.26, Mahalanobis                                               |
| $F_3$ Hjorth complexity ($c_b$) | 0.1022     | 66.61                                                    | 60.82, Mahalanobis                                               |
| $F_4$ interquartile range (IQR) | 0.2383    | 65.07                                                    | 63.62, LDA/Diaglinear                                           |
| $F_5$ variance ($\sigma^2$) | 0.0453    | 63.57                                                    | 65.58, LDA/Diaglinear                                           |
| $F_6$ average spectral power ($P$) | 0.1385 | 60.51                                                    | 61.58, Mahalanobis                                               |
| $F_7$ DFA ($\alpha$) | 0.1989         | 60.14                                                    | 61.28, Mahalanobis                                               |
| $F_8$ kurtosis ($\beta$) | -0.0637      | 58.06                                                    | 62.64, Mahalanobis                                               |
| $F_9$ Hjorth mobility ($m_a$) | 0.0064     | 57.45                                                    | 61.44, Mahalanobis                                               |
| $F_{10}$ skewness ($\gamma$) | -0.5731 | 54.55                                                    | 62.09, Mahalanobis                                               |
| $F_{11}$ Hurst exponent ($H$) | 0.0321   | 52.38                                                    | 61.40, Mahalanobis                                               |
mean and covariance matrices for each of the classes are denoted by $(\mu_i, S_i)$ and $\mu_0$ is the global mean vector. The scatter matrix extends the concept of class separability using FDR from binary classification to multi-class problems.

The scatter matrices value in table 3 provide an insight into how good the separation between the four classes (stimuli) are using the individual features. From table 3, we can see that the signal ‘mean’ on its own has the best classification result for the six binary combinations of four stimuli. However, as we have extracted the features from the raw non-stationary plant electrical signals, the mean is not a very reliable feature to base any conclusions on, because it can be influenced by various artefacts and noise during measurement or from various environmental factors (e.g. sudden gust of breeze could shake the electrodes connected to the plant body). The next five best features (best average accuracies given in table 3), when taken individually, are wavelet packet entropy, Hjorth complexity, IQR, variance and average spectral power, respectively. From now on, we will only consider these features as the top five features. In table 3, we also report the best achievable accuracy along with the best classifier using each of the single features to discriminate the four stimuli within a ‘one versus rest’ strategy. This highlights the possibility of isolating one particular class from the other classes using a single feature, with a certain degree of confidence.

So far we have seen the averaged results of classification for six binary stimuli combinations using individual features. We next find the best classified stimuli combination using only the top five individual features and using the five variants of the discriminant analysis classifiers, as mentioned above. As a result, we obtained five classification accuracies (for five individual features) for every classifier for each of the six binary stimuli combinations. That results in 25 classification accuracies for each of the six binary stimuli combinations. These 25 results were averaged for each stimuli combination and given in table 4 which shows the best discrimination possible is for H2SO4 and O3 with classification accuracy over 73%. Additionally, discrimination between NaCl (both concentrations) and O3/H2SO4 also shows promising results with accuracy over 65% and 63%, respectively.

The average classification results presented in table 4 encourage us to look at the best results achieved using individual features, for each stimuli combination, so that we can see whether there is a consistent feature giving good classification results. This is shown in table 5 from where it is evident that F3 (Hjorth complexity) gives the best result for three different binary stimuli combinations with an accuracy over 74%. Overall, the best accuracy is achieved for classification between H2SO4 and O3, with an accuracy of more than 94% using F2 (Wentropy) and QDA classifier. Although in table 4, the discrimination between NaCl and O3/H2SO4 are shown in terms of the average accuracy, which might seem to be relatively low (63 or 65%), the best cases for such a discrimination can be found in table 5 (accuracies of more than 78% and more than 72%, respectively) between the same set of stimuli. Also from figure 5, we can see that though skewness shows good discrimination between H2SO4 and other stimuli, from table 3 we can see that the average classification accuracy using skewness as an individual feature is very low. This is due to the fact that skewness on its own did not give good classification results between other remaining stimuli combinations.

### 3.4. Classification using feature pairs

Next, we looked at the effect of all possible feature pairs using 11 individual features (totalling 55 independent feature pairs) on the classification results between six different stimuli combinations. These classification accuracies are shown in figure 6 along with the difference in accuracy (error) when the background is not subtracted as discussed in earlier section. The features mentioned as $\{1,2,\ldots,11\}$ in figure 6 are the features designated by $(f_1,f_2,\ldots,f_{11})$, respectively, in table 2. As we ignored mean as a feature in the previous section, we explored the effect of taking binary combinations of the next five individual features (F2 through F6, as mentioned in table 3) on the classification accuracy. The results obtained using each of these bivariate features (pairs), using all the five classifier variants were averaged and given in table 6, which are found to be better than the averaged results obtained using just univariate features as given in table 4.

By this exploration, we wanted to find out whether there is any improvement on the classification accuracy when a feature pair is used rather than just an individual feature. From table 6, we can see that classification accuracy is improved for all stimuli combinations except NaCl 5 ml versus H2SO4. We can also observe from table 6 that the top two best accuracies are obtained for stimuli combinations of NaCl 10 ml versus O3 and H2SO4 versus O3. Now, let us look at the best feature pair(s), among all 55 bivariate feature pairs, as given in table 7. We notice that a combination of F4 (IQR) and F5 (variance) results in the best classification accuracy for four out of six different stimuli combinations. For the remaining two stimuli combinations, a feature pair of F4 and F6 (average spectral power) gives the best classification accuracies.

### 3.5. Finding the most reliable combination of feature or feature pair and classifier variant

So far, we have found that individual features F2, F3, F5 and F6 and feature pairs F4-F5 and F4-F6 produced the best classification results for one or more (out of the six) stimuli combinations. We now explore these features and feature pairs for all stimuli combinations. Table 8 gives the results of classification when we used just F2, F3, F5 and F6 as an individual feature using all classifier variants for all binary stimuli combinations. Similarly, table 9 gives the results using the feature pairs F4-F5 and F4-F6 for all the six stimuli combinations, using all the five classifier variants. These results will help us choose the right classifier and decide the feature or feature pair which provides the best average accuracy for all the binary combinations of stimuli.
From table 8, we note that using just F2 or F3 provides consistently better average classification accuracies than using F8 or F9. It is also noted that although F2 provides a better classification for the stimuli combinations NaCl 10 ml versus O3 and O3 versus H2SO4, F3 provides more consistent and better results for the remaining stimuli combinations. While considering a single feature for discriminating the four stimuli, the best average result (73%) could be obtained using the F2 (Wentropy) feature and Mahalanobis classifier, although it is highly correlated with the signal mean (F1) as shown in table 2. As mean is a feature was ignored owing to its susceptibility to artefacts, therefore, we also ignore Wentropy and instead propose Hjorth complexity as the best individual feature for achieving good average classification accuracy.

When using bivariate feature pairs, it is evident from table 9 that the top two classification accuracies (more than 73%) are obtained using the F4–F5 combination and Diagquadratic and QDA as classifiers, respectively. Both these top bivariate classification results (average accuracy of 69.65% across all stimuli and classifiers) are better than that obtained in the univariate case in table 8 (average accuracy of 62.98% across all stimuli and classifiers). Although again from table 2, we realize that the IQR and variance are highly correlated with each other but as we are achieving a good result in terms of classification using these two features, we note that calculating IQR and variance from a block of 1000 samples of raw non-stationary plant electrical signal, along with QDA or Diagquadratic classifier will provide consistently good results in terms of classifying which external stimuli caused the particular signature in the plant electrical signal.

Figure 5. Univariate histograms of each of the 11 features for four different stimuli (with background subtraction). (Online version in colour.)
Table 7. Best accuracy for each stimulus combination using two features (best separability between different stimulus combinations).

| stimuli       | NaCl 5 ml | NaCl 10 ml | H₂SO₄ | O₃        |
|---------------|-----------|------------|-------|-----------|
| NaCl 5 ml     | —         | 63.18% (F₄–F₅ with Diaglinear) | 65.87% (F₄–F₅ with linear) | 82.69% (F₄–F₅ with Diaglinear) |
| NaCl 10 ml    | *         | —          | 73.18% (F₄–F₅ with Diagquadratic) | 92.06% (F₄–F₅ with Mahalanobis) |
| H₂SO₄         | *         | *          | —     | —         |
| O₃            | *         | *          |       |           |

Table 8. Accuracy of different classifiers for six stimuli combinations (in %) using the best individual features.

| individual feature | classifier variant | NaCl 5 ml versus 10 ml | NaCl 5 ml versus H₂SO₄ | NaCl 5 ml versus O₃ | NaCl 10 ml versus H₂SO₄ | O₃ versus H₂SO₄ | average accuracy (%) |
|--------------------|--------------------|------------------------|------------------------|---------------------|--------------------------|------------------|----------------------|
| F₂ (entropy)       | LDA                | 55.3                   | 66.4                   | 73.4                | 77.6                     | 59.5             | 82.8                 | 69.2                 |
|                    | QDA                | 52.2                   | 67.6                   | 62                  | 74                       | 56.4             | 95                   | 67.9                 |
|                    | Diaglinear         | 55.3                   | 66.4                   | 73.4                | 77.6                     | 59.5             | 82.8                 | 69.2                 |
|                    | Diagquadratic      | 52.2                   | 67.6                   | 62                  | 74                       | 67.3             | 95                   | 69.7                 |
|                    | Mahalanobis        | 55.5                   | 73.1                   | 73.7                | 78.2                     | 63.8             | 94.4                 | 73.1                 |
| F₃ (Hjorth complexity) | LDA              | 74.4                   | 73.9                   | 78.9                | 66                       | 68.3             | 66.9                 | 71.4                 |
|                    | QDA                | 74.1                   | 47.1                   | 61.6                | 71.5                     | 67.5             | 41.4                 | 60.6                 |
|                    | Diaglinear         | 74.4                   | 73.9                   | 78.9                | 66                       | 68.3             | 66.9                 | 71.4                 |
|                    | Diagquadratic      | 74.1                   | 47.1                   | 61.6                | 71.5                     | 67.5             | 41.8                 | 60.6                 |
|                    | Mahalanobis        | 74.4                   | 75.1                   | 62.4                | 51.1                     | 69.4             | 81.5                 | 69                   |
| F₄ (kurtosis)      | LDA                | 57.1                   | 66.5                   | 57.6                | 60.5                     | 72.1             | 66.1                 | 63.3                 |
|                    | QDA                | 47.8                   | 38.4                   | 69.3                | 47.1                     | 71.8             | 22.5                 | 49.5                 |
|                    | Diaglinear         | 57.1                   | 66.5                   | 57.6                | 60.5                     | 72.1             | 66.1                 | 63.3                 |
|                    | Diagquadratic      | 47.8                   | 38.4                   | 69.3                | 47.1                     | 71.8             | 22.5                 | 49.5                 |
|                    | Mahalanobis        | 57.7                   | 58.2                   | 38.5                | 81.3                     | 71.3             | 81                   | 64.7                 |
| F₉ (Hjorth mobility) | LDA              | 60.4                   | 73.9                   | 68.5                | 66                       | 56               | 35.8                 | 60.1                 |
|                    | QDA                | 49.7                   | 47.7                   | 76.4                | 82.3                     | 48.7             | 81.6                 | 64.4                 |
|                    | Diaglinear         | 60.4                   | 48.8                   | 68.5                | 66                       | 56               | 35.8                 | 55.9                 |
|                    | Diagquadratic      | 49.7                   | 47.7                   | 76.4                | 82.3                     | 48.7             | 81.6                 | 64.4                 |
|                    | Mahalanobis        | 66.2                   | 54.6                   | 30.1                | 24.7                     | 58.4             | 20.5                 | 42.4                 |

Figure 6. (a) Classification accuracy for different feature combinations with background information removed; (b) deterioration in accuracy for the features without background information removed. (Online version in colour.)
In figure 7, except the first subplot with $f_2-f_3$, the rest of the combinations are almost uncorrelated and still give good classification performance. Thus as a reliable measure of analysis, it has been found that the variance and skewness calculated from a block of 1000 samples of plant electrical signal will be able to give an average (over all six stimuli combinations and using all five discriminant classifiers) accuracy of 70% during binary classification of the stimuli. It is to be noted that in the bivariate classification scheme, the mean ($F_1$) has not been considered as one of the features. Also, the best bivariate accuracies were achieved involving the variance ($F_2$) along with all the other features ($F_4-F_{11}$) in figure 7, while ignoring the $F_2-F_3$ combination owing to their high correlation of approx. 0.01 in table 2).

We next explore some pairs of uncorrelated features for classification by looking at the 12 next best average classification accuracies (obtained across all stimuli combinations and using all five different classifiers) as shown through two-dimensional normalized histograms (volume being unity) plots showing the separation of the four stimuli in figure 7. Average accuracy obtained (over all stimuli combinations and classifiers) using particular feature pairs (denoted by $f_{ij}$, $f_{ij} \ldots f_{ij}$, as described in table 2) are also mentioned in the title of each subplot in figure 7. It is observed that the second best average classification accuracy is achieved using variance and skewness as features that are almost uncorrelated (correlation of approx. 0.01 in table 2).

Table 9. Accuracy of different classifiers for six stimuli combinations (in %) using the best feature pairs.

| best feature set | classifiers | NaCl 5 ml versus 10 ml | NaCl 5 ml versus $H_2SO_4$ | NaCl 5 ml versus $O_3$ | NaCl 10 ml versus $O_3$ | NaCl 10 ml versus $H_2SO_4$ | $O_3$ versus $H_2SO_4$ | average accuracy (%) |
|------------------|-------------|------------------------|-----------------------------|------------------------|--------------------------|-----------------------------|------------------------|---------------------|
| $F_4-F_5$        | LDA         | 56.61                  | 62.61                       | 82.53                  | 81.57                    | 69.24                       | 85.09                  | 72.94               |
| (IQR-variance)   | QDA         | 57.78                  | 61.62                       | 82.24                  | 86.06                    | 64.69                       | 87.49                  | 73.31               |
|                  | Diaglinear  | 63.17                  | 53.8                        | 82.7                   | 83.47                    | 62.06                       | 80.33                  | 70.92               |
|                  | Diagquadratic | 60.34                | 58.43                       | 82                     | 86.08                    | 73.19                       | 81.98                  | 73.67               |
|                  | Mahalanobis | 62.17                  | 50.23                       | 80.24                  | 92.07                    | 53.64                       | 78.91                  | 69.54               |
| $F_4-F_6$        | LDA         | 56.88                  | 65.87                       | 71.61                  | 70.60                    | 67.94                       | 81.27                  | 68.94               |
| (IQR-average)    | QDA         | 57.82                  | 57.01                       | 73.89                  | 81                      | 65.19                       | 78.48                  | 68.9                |
|                  | Diaglinear  | 63.19                  | 54.59                       | 68.67                  | 78.16                    | 64.92                       | 71.39                  | 66.82               |
|                  | Diagquadratic | 58.11                | 60.57                       | 79.19                  | 75.70                    | 67.96                       | 79.66                  | 68.31               |
|                  | Mahalanobis | 62.61                  | 52.99                       | 62.72                  | 79.62                    | 58.08                       | 60.84                  | 63.20               |
4. Discussion

In our exploration, the data from two channels per plant (per experiment) were used to record the electrical response, and then statistical features were calculated from both the channels and pooled together. Here, the location on the plant body for the data extraction was ignored, as the work was primarily focused more on the possibility of classification of applied external stimuli from the extracted plant electrical signal. Similarly, the effects of a different species of plant to study the four stimuli have also been ignored, except the introduction of an additional species (cucumber) for the ozone stimulus. The idea behind developing an external stimuli classification scheme, based on plant electrical responses is focused on generic plant signal behaviour and not of a specific species. However, such isolation forms a very good study and could be taken up as future work. There might be some possibility of confounding effects based on the position of the electrodes and plant species in any classification scheme. But such confounding effects will be minimal owing to the large number of data samples as shown in table 1 and the use of cross-validation schemes to test the performance of the discriminant analysis classifiers. Also we did not use kernel-based nonlinear classifiers like SVM which could over-fit these plant-specific characteristics and still give good classification results, rendering the loss of generalizing capability of the classifier.

Moreover, the present classification scheme is based on the raw non-stationary plant signal. In bio-signal processing literature [11], the use of a high-pass filter is recommended to make a bio-signal stationary instead of extracting features from the raw non-stationary signal. But there is also the possibility with ad hoc filtering that some useful information in the data may get lost as the cut-off frequency for plant signal processing is not yet known. That is why we considered the features from the post-stimulus signal to train the classifier by removing any possible bias of the channel or plant using incremental features, i.e. using the mean of the features in the pre-stimulus part. The segmentation of the signal in a block of 1000 samples also disregards the temporal information of the stimuli, as we primarily tried to answer the question of whether classification is indeed possible by looking at any segment of the post-stimulus part of the signal. Also, in a realistic scenario, we would not know when the response to a particular stimulus started. So we need to base our classification on the in-coming stream of live data.

5. Conclusion

Our exploration using raw electrical signals from plants provides a platform for realizing a plant signal-based biosensor to classify the environmental stimuli. The classification scheme was based on 11 statistical features extracted from segmented plant electrical signals, followed by feature ranking and rigorous univariate and bivariate feature-based classification using five different discriminant analysis classifiers. External stimuli-like \( \text{H}_2\text{SO}_4 \), \( \text{O}_2 \) and \( \text{NaCl} \) in two different amounts (5 ml and 10 ml) have been classified using the adopted machine-learning approach with 11 statistical features, capturing both the stationary and non-stationary behaviour of the signal. The classification has yielded a best average accuracy of 70% (across all stimuli and five classifier variants using variance and skewness as feature pairs) and the best individual accuracy of 73.67% (across all stimuli and using variance and IQR as feature pairs in Diagquadratic classifier). The very fact that, by looking at the statistical features of plant electrical response, we can successfully detect which stimuli caused the signal is quite promising. This will not only open the possibility of remotely monitoring the environment of a large geographical area, but will also help in taking timely preventive measures for natural or man-made disasters.

Data accessibility. The experimental data are available in the PLEASED website at http://pleased-fp7.eu/?page_id=253.

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