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Dynamic Phases of Active Matter Systems with Quenched Disorder

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Depinning and nonequilibrium transitions within sliding states in systems driven over quenched disorder arise across a wide spectrum of size scales ranging from atomic friction at the nanoscale, flux motion in type-II superconductors at the mesoscale, colloidal motion in disordered media at the microscale, and plate tectonics at geological length scales. Here we show that active matter or self-propelled particles interacting with quenched disorder under an external drive represents a new class of system that can also exhibit pinning-depinning phenomena, plastic flow phases, and nonequilibrium sliding transitions that are correlated with distinct morphologies and velocity-force curve signatures. When interactions with the substrate are strong, a homogeneous pinned liquid phase forms that depins plastically into a uniform disordered phase and then dynamically transitions first into a moving stripe coexisting with a pinned liquid and then into a moving phase separated state at higher drives. We numerically map the resulting dynamical phase diagrams as a function of external drive, substrate interaction strength, and self-propulsion correlation length. These phases can be observed for active matter moving through random disorder. Our results indicate that intrinsically nonequilibrium systems can exhibit additional nonequilibrium transitions when subjected to an external drive.

I. INTRODUCTION

Depinning phenomena and dynamic phases of collective transport through quenched disorder \cite{1, 2} arise in a wide range of condensed matter systems including flux lines in superconductors \cite{3–9}, sliding charge density waves \cite{10}, moving electron crystals \cite{11, 12}, magnetic skyrmions \cite{13, 14}, and driven pattern forming systems such as electronic states with competing interactions \cite{15}.

In materials science systems such dynamics are relevant to sliding friction \cite{16}, dislocation motion \cite{17}, yielding transitions \cite{18, 19}, and models of fault lines and earthquakes \cite{20, 21}. In soft matter, similar dynamics occur in the depinning of contact lines \cite{22, 23}, driven colloidal motion on disordered substrates \cite{24–26}, or sliding of incommensurate colloidal structures on ordered substrates \cite{27, 28}.

Typically, these systems are in the pinned state at small external drives, and as the drive increases, a transition to a moving state occurs at a specific critical value of the external force \cite{1, 2}. At higher drives, distinct types of sliding motions can appear along with transitions between different dynamic states that can be deduced from features in the velocity-force curves. The flow can be plastic or disordered \cite{1–5, 8}, with the particles moving through riverlike channels \cite{24–26}, or elastic, where the particles maintain the same neighbors while moving \cite{1, 3, 24}.

Transitions from disordered to more ordered or coherent flow can occur \cite{3–6, 8, 9}, such as from plastic flow to a moving smectic state \cite{6–9}. Such transitions are associated with changes in the moving structure morphologies, the density of topological defects \cite{4, 8, 9, 14, 24}, and the noise fluctuations \cite{5, 8}.

In all of the systems mentioned above, an external driving force produces a nonequilibrium condition. Other types of nonequilibrium systems that involve no external driving force include self-propelled or active matter systems. These may be biological systems, such as swimming bacteria, or artificial swimmers, such as self-propelled colloidal systems, each of which can exhibit distinct nonequilibrium phases as a function of the activity or particle density \cite{29, 30}.

Many types of active matter systems can be effectively modeled as a collection of sterically interacting disks undergoing driven Brownian diffusion \cite{31–35} or run-and-tumble dynamics \cite{35–38}. These disks can form uniform liquid states as well as phase separated states in which dense disk clusters are separated by a low density disk gas. An open question is whether such systems would exhibit depinning transitions and different types of sliding states if an external drive were applied when the disks are coupled to a random substrate, as the driven dynamics of particles interacting with obstacles generally are distinct from those of particles on random pinning substrates. Previous studies of active matter systems driven through obstacle arrays showed that the average drift mobility varies non-monotonically with increasing activity, dropping when the system forms a phase-separated clump state \cite{38}. Other studies of active matter involving swarming or Vicsek flocking models moving over disordered substrates in the absence of an external drive showed that there can be an optimal noise at which flocking occurs \cite{39} as well as transitions from flocking to non-flocking behavior \cite{40}.

Here we use large scale GPU-based computer simulations to characterize the different states of run-and-tumble disks driven over a random pinning substrate, and show that a rich variety of distinct dynamical phases are possible that can be identified by the morphologies of the moving structures as well as by features in bulk transport properties. Despite the additional complexity introduced by the self-propulsion, we find several generic features in
the dynamic phase diagrams that are similar to those observed for non-active driven systems such as superconducting vortex lattices, including a disorder-order transition at higher drives. In the limit of no quenched disorder, we find a cluster or phase-separated state, while in the presence of strong quenched disorder, the system forms a uniform pinned liquid state which undergoes plastic depinning as the drive is increased, followed at higher drives by a transition to a stripe state coexisting with the pinned liquid state. At even higher drives, there is a transition to a more fully phase separated state. We also find strong differences in the dynamic phases for pinning arrays compared to those observed in obstacle arrays, where only a limited number of dynamic phases occur.

The organization of this paper is as follows. In Section III we describe the dynamic phases that arise for active run-and-tumble disks driven over pinning arrays. The five generic phases that emerge for high activity, shown in Section III A, are the pinned phase I, the disordered plastic flow phase II, the moving cluster-stripe phase III coexisting with pinned disks, and two phases in which all of the disks are moving: the moving cluster or phase separated phase IV and the moving disordered or liquid phase V. We demonstrate the evolution of these phases as the pinning strength is varied, and find that the extent of the pinned phase, the plastic disordered flow phase, and the stripe phase increase with increasing pinning strength. In the limit of zero drive we observe a transition from a phase separated state to a disordered pinned state as the pinning force increases. The different states can be identified by analyzing changes in the size of the clusters, the fraction of disks with six neighbors, and the velocity-force curves. We compare the evolution of the dynamic phases with pinning strength to that observed for vortices in type-II superconductors and other driven particle systems. In Section III B we explore the effects on the dynamic phases of changing the activity from the non-active or Brownian limit to the highly active limit, and find that there is a critical activity level or run length below which phases III and IV do not occur. In Section IV we show how the driven phases change when the pinning sites are replaced by obstacles. There is still a transition from a phase separated to a disordered phase as a function of obstacle density in the zero drive limit; however, we find no dynamical phase transitions within the moving phase, and the cluster size and transport curves show only smooth changes with increasing obstacle density. We provide a summary of our results in Section V.

II. SIMULATION

We perform a simulation of $N = 5000$ to $N = 24000$ run-and-tumble disks in a system with periodic boundary conditions of size $L \times L$ with $L = 300$. The disks have a short range repulsive interaction modeled as a harmonic spring force $F_{\text{int}} = \Theta(d - 2R)k(d - 2R)\hat{d}$, where $d$ is the distance between the centers of the disks, $\hat{d}$ is the displacement vector between the disk centers, $k = 20.0$ is the spring constant, and $\Theta(x)$ is the Heaviside function. We use a disk radius of $R = 1.0$. The system density $\phi$ is defined by the area coverage of disks, $\phi = N\pi R^2/L^2$, giving us a range of $\phi = 0.1745$ to $\phi = 0.8375$. We randomly place $N_p$ non-overlapping pinning sites which are modeled as parabolic traps that exert a force on the disks of the form $F_p = F_p(r/R_p)\Theta(r - R_p)\hat{r}$, where $\hat{r}$ is the displacement vector from the pinning site center to the disk center, $r = |r|$, $F_p$ is the maximum pinning force, and $R_p$ is the pinning site radius. We set $R_p = 0.5$ to ensure that at most one disk can be pinned by a given pinning site. We apply a uniform external drive $F_D = F_D\hat{x}$ on each disk in the $x$-direction and measure the resulting average drift velocity per disk in the direction of the drive $\langle V \rangle = N^{-1}\sum_{i=0}^{N}\langle v_i \cdot \hat{x} \rangle$ to produce velocity-force curves.

The disk dynamics is obtained by integrating the following overdamped equation of motion: $\eta d\mathbf{r}/dt = F_{\text{int}} + F_m + F_p + F_D$, where $\eta = 1$ is the drag coefficient. The disk self-propulsion is produced by the motor force $F_m$, which acts on a given disk in a fixed randomly chosen direction for a run time $\tau$ that is chosen from a uniform random distribution over the range $[\tau_r, 2\tau_r]$. After $\tau$ simulation time steps have elapsed, the motor force instantly reorients to a new randomly chosen direction, which it maintains for the next $\tau$ simulation time steps before reorienting again. In the absence of other disks, pinning sites, or obstacles, a disk would move a distance $D$ during one running time, where $D$ is uniformly randomly distributed over the range $[\tau, 2\tau]$. We use $F_m = 1.0$ and run times ranging from $\tau_r = 1000$ to $\tau_r = 2.4 \times 10^6$ simulation steps, with a simulation time step of $\delta t = 0.001$. To initialize the system, we place the disks in random configurations and increase $F_D$ by increments of $\delta F_D = 0.25$, spending $1 \times 10^6$ simulation time steps at each increment. This protocol allows us to ensure that the system has reached a steady state before we perform our measurements. An alternative protocol is to increase the driving force continuously. If the rate of increase is slow, both protocols produce the same results and the behavior of the system is not hysteretic. Rapid rates of change of the driving force can induce hysteresis and other rate-dependent phenomena similar to that observed in other systems driven over random disorder that exhibit depinning transitions [2]; however, an exploration of such effects is beyond the scope of this work. Rate-dependent effects may be particularly enhanced in active matter systems as there is a time scale associated with the run time. We allow our system to remain at each driving force increment value much longer than any of the run times we consider in order to ensure that we have reached a steady state.
III. DYNAMIC PHASES AND TRANSPORT ON PINNING SITES

A. Changing Disk Density and Pinning Strength

In Fig. 1 we illustrate the disk locations for a system with $\phi = 0.55$, $r_1 = 300$, $N/N_p = 2.0$, and $F_p = 5.0$. For these values of $\phi$ and $r_1$, in the absence of pinning the system forms a phase separated state in which the disks condense into a single large dense cluster. When pinning is present, Fig. 1(a) shows that at $F_D = 0$, the system forms a homogeneous disordered phase. We identify disks that are in contact with one another using the Luding and Herrmann cluster algorithm [41], and plot the largest cluster in blue, the second largest cluster in red, and the next largest clusters in green, purple, and orange. In Fig. 1(a) for $F_D = 0$, the largest cluster percolates across the entire sample. At $F_D = 0.5$ in Fig. 1(b), we observe a plastic flow state, as indicated by the riverlike disk trajectories, in which the overall disk density remains uniform. As $F_D$ increases, a transition occurs into a moving stripe state as shown in Fig. 1(c) for $F_D = 3.25$. The dense stripe is oriented parallel to the driving force and moves in the positive $x$ direction. The disks that are not in the dense phase are directly trapped by the pinning sites. As $F_D$ approaches $F_p$, more of the pinned disks become mobile and the system enters the fully phase separated state illustrated in Fig. 1(d) for $F_D = 6.0$, where a single large clump appears that translates in the direction of drive but has no particular orientation with respect to the driving direction.

In Fig. 2(a) we plot the velocity-force curves for the system in Fig. 1 at disk densities ranging from $\phi = 0.1745$ to $\phi = 0.8375$ in increments of $\delta \phi = 0.035$, while in Fig. 2(b) we show the corresponding $d\langle V \rangle / dF_D$ curves. The letters a to d indicate the values of $F_D$ at which the images in Fig. 1 were obtained for the $\phi = 0.55$ which corresponds to the $16k$ curve. (b) The corresponding $d\langle V \rangle / dF_D$ curves. (c) The size of the largest cluster $\tilde{C}_L$ vs $F_D$. The dashed line indicates the transition into the moving stripe state, and the solid line denotes the transition to the moving phase separated state. (d) The number of six-fold coordinated disks $\tilde{P}_6$ vs $F_D$. The error bars in this and all remaining figures are smaller than the size of the symbols.
the images in Fig. 1 were obtained for the $\phi = 0.55$ sample (which corresponds to 16,000 disks), demonstrating that the different phases correlate with distinct features in the transport curves. Previous studies of superconducting vortex systems showed that a peak in $d(V)/dF_D$, the derivative of the velocity-force curve, is associated with a dynamical phase transition from plastic flow to a moving lattice state [2, 3, 8]. In more complex systems, such as driven pattern forming systems, multiple peaks in the $d(V)/dF_D$ curves coincide with multiple transitions in the structure of the moving state [42, 43]. In Fig. 2(a), a depinning transition occurs at a critical driving force $F_c$ which shifts to lower values as $\phi$ increases. The $d(V)/dF_D$ curves in Fig. 2(b) have a double peak feature, with the largest peak near $F_D = 4.0$ and a smaller peak at lower values of $F_D$. Both peak features become less distinct as $\phi$ increases. The transition from a pinned state to plastic flow occurs at the point at which $d(V)/dF_D$ first rises above zero, while the moving stripe phase appears just above the first peak in $d(V)/dF_D$. The second peak in $d(V)/dF_D$ is associated with a transition to a moving fully phase separated state or to a uniformly dense state in which all the disks are in motion.

In Fig. 2(c,d) we plot the size of the largest cluster $C_L$ and the number of six-fold coordinated disks $P_6$, obtained from a Voronoi tessellation, versus $F_D$ for the system in Fig. 2(a,b). For clarity, both $C_L$ and $P_6$ are plotted in terms of the total number of disks and are not normalized to range between 0 and 1. For $\phi < 0.314$, the system is in the moving disordered state for all values of $F_D$. For $F_D = 0$, there is a pinned labyrinth phase similar to that shown in Fig. 1(a) for $\phi > 0.525$, while for $\phi < 0.525$ there is a pinned liquid state similar to that illustrated in Fig. 3(c) at $\phi = 0.35$. At low drives, a drop in $C_L$ occurs when the labyrinth phase breaks apart into a moving disordered phase, as illustrated in Fig. 1(b). The dashed line highlights an increase in $C_L$ that occurs when the system enters a moving stripe phase. In Fig. 2(c) the thick solid line highlights an increase in $C_L$ that occurs near $F_D = 4.0$, which is also the location of the largest peak in $d(V)/dF_D$. In Fig. 2(d), there is an upward jump in $P_6$ near $F_D = 4.0$, marked with a solid line, at the transition into the moving fully phase separated state. At lower $F_D$ there is a smaller jump in $P_6$ marked with a dashed line connected with the transition into a moving stripe state. There is an increase in $P_6$ whenever dense regions of disks form since the densely packed regions have triangular ordering with disks that are mostly six-fold coordinated. We note that in the labyrinth phase, $C_L$ can be large since a cluster can percolate across the entire system as illustrated in Fig. 1(a), but $P_6$ remains low since the disks within the labyrinth are disordered.

In Fig. 3(a) we illustrate the pinned cluster state at $F_D = 0$ and $\phi = 0.8375$, while Fig. 3(b) shows the moving stripe state at the same disk density for $F_D = 1.5$. The stripe structure moves in the positive $x$ direction, parallel to the drive. Figure 3(c) shows the pinned liquid phase at $F_D = 0$ and $\phi = 0.35$, where the clusters are absent, and Fig. 3(d) illustrates the moving phase separated state at $\phi = 0.35$ and $F_D = 5.0$.

From the features in $C_L$, $P_6$, and the transport curves in Fig. 2, we identify distinct dynamic phases as plotted in Fig. 4. As a function of $F_D$ versus $\phi$, shown in Fig. 4(a), we find five dynamic phases, marked I through V. There is a transition out of phase I, the pinned phase, at the depinning threshold $F_c$, which drops to lower $F_D$ with increasing $\phi$. A dashed line marks the transition between $\phi < 0.525$, where the pinned clusters do not percolate and a pinned liquid of the type shown in Fig. 3(c) forms, and $\phi > 0.525$, where a pinned percolating cluster appears as illustrated in Fig. 1(a) and Fig. 3(a). In phase II, plastic flow of the type illustrated in Fig. 1(b) occurs, and the disk density is mostly homogeneous. Phase III, the moving stripe phase, is shown in Fig. 1(c) and Fig. 3(b). Figures 1(d) and 3(d) illustrate phase IV, the moving fully phase separated state, while in phase V, the moving liquid state, no clustering occurs but all the disks are moving.

We have also examined the dynamic phases as a function of the pinning strength $F_p$. In Fig. 5(a) we plot $d(V)/dF_p$ versus $F_D$ for a system with $\phi = 0.55$ and
**FIG. 4:** (a) The dynamic phase diagram as a function of $F_D$ vs $\phi$ constructed from the features in Fig. 2 for a sample with $F_p = 5.0$, $N_p = 8000$, and $r_l = 300$. I: pinned phase; II: plastic flow phase; III: moving stripe phase; IV: moving fully phase separated state; V: moving liquid phase. The dashed line in phase I indicates the separation between a pinned liquid and a pinned labyrinth state. (b) The dynamic phase diagram as a function of $F_D$ vs $F_p$ for a sample with $\phi = 0.55$, $N/N_p = 2.0$, and $r_l = 300$. The phases I through V are marked as above. Phase VI is the moving phase separated state in which some disks can be temporarily pinned.

$N/N_p = 2.0$ over the range $F_p = 0$ to $F_p = 9.0$. A double peak in $d(V)/dF_D$ occurs only when $F_p > 1.5$, and both peaks shift to higher values of $F_D$ with increasing $F_p$. Figure 5(b) shows the corresponding normalized fraction of sixfold coordinated disks $P_6 = P_6/N$ versus $F_D$. For $F_p > 3.5$, the disks are disordered and $P_6 \approx 0.5$. When the system enters phase III, a feature appears near $P_6 = 0.75$, and there is a jump up in $P_6$ at the onset of phase IV. For low pinning strengths of $F_p < 2.75$, a moving phase separated state called phase VI appears in which some disks can be temporarily pinned, while for large enough $F_D$ all the disks are moving and the system enters phase IV, the flowing state. The dynamic phase diagram as a function of $F_D$ versus $F_p$ in Figure 4(b) indicates that phase III flow only occurs for $F_p > 2.0$, while phases I and III grow in extent with increasing $F_p$. In Fig. 4(b) at $F_D = 0.0$ there is a transition from phase VI, the pinned phase separated state, to the disordered pinned phase I for $F_p > 2.0$. It may be possible to analyze several of these phases in terms of driven diffusion or driven Ising lattice models by mapping the activity into the model.

The general features of the $F_D$ versus $F_p$ dynamic phase diagram in Fig. 4 exhibit several similarities to the $F_D$ versus $F_p$ dynamic phase diagram found for vortices in type-II superconductors [1, 2]. In the vortex system, there is an analogous transition from a pinned phase to a plastic flow phase which shifts to higher $F_D$ with increasing $F_p$. There is also a transition from the plastic flow phase to a moving ordered phase in which all of the vortices are moving, which is analogous to the II-IV transition we observe. There is no equivalent to our phase III in the vortex system since a moving vortex crystal cannot coexist with pinned vortices.

**B. Changing Run Length and Pinning Density**

In Fig. 6(b) we plot the velocity-force curves and in Fig. 6(a) we show the corresponding $d(V)/dF_D$ curves for a system with $F_p = 5.0$, $\phi = 0.55$, and $N/N_p = 2$ for varied run lengths from $r_l = 1.0$ to $r_l = 1200$. The curves follow each other closely except for the second peak in $d(V)/dF_D$, which increases in magnitude with increasing $r_l$. The second peak is absent at lower $r_l$ when a transition from phase II to phase V occurs, but materializes at larger $r_l$ once a transition from phase III to phase IV begins to occur. In Fig. 6(c) we plot the corresponding $P_6$ versus $F_D$ curves which show the onset of the transition into region IV in the form of an increase in $P_6$. In Fig. 7(a), we show the dynamic phase diagram as a function of $F_D$ versus $r_l$ for the system in Fig. 6, where phases
IV and III only occur for \( r_l > 60 \). For \( r_l < 60 \), phase IV, the moving phase separated state, disappears, and the system passes directly from phase II plastic flow to the phase V moving liquid. Here, the line marking the phase II to phase V transition remains flat at \( F_D = F_p = 5.0 \). These results indicate that the generic phases we observe are robust for \( r_l \) values both larger and smaller than the system size \( L \). We have performed simulations on samples of smaller size and find the same features in the phase diagram, since a key parameter is the strength of the pinning relative to the driving force, which is independent of sample size.

We have also examined the case of fixed \( \phi = 0.55 \) and \( r_l = 300 \) to obtain the dynamic phase diagram as a function of \( F_D \) versus \( N_p \), shown in Fig. 7(b). Phase III diminishes in width until \( N_p/N = 1.0 \). For larger \( N_p \), there is a direct transition from phase II to phase IV, and phase III flow disappears. Our results indicate that the dynamic phases we observe persist over a wide range of parameters and represent generic features of this class of system.

**IV. DYNAMICS IN OBSTACLE ARRAYS**

Active disks moving through obstacle arrays have a very different behavior than that described in Section III for active disks in pinning arrays. To explore this, we prepare an obstacle landscape in which the obstacles are modeled as immobile disks with a radius of 1.0. We consider a system with \( r_l = 300 \), a mobile disk density of \( \phi = 0.55 \), and \( N_o \) obstacles. An obstacle-free system at this disk density and running length \( r_l \) forms a phase separated state for \( F_D = 0 \). As we increase the number of obstacles \( N_o \), we find a transition from a phase separated state to a uniform liquid state, as indicated in the plot of the normalized value of \( C_L \) versus \( N_o \) in the inset of Fig. 8(a). We show snapshots of the disk and obstacle positions in Fig. 9. At \( F_D = 0 \), Fig. 9(a) indicates that a sample containing \( N_o = 8000 \) obstacles is disordered, while Fig. 9(c) shows that when \( N_o = 2000 \) obstacles are present, the system is density phase separated. In Fig. 8 we plot the velocity \( \langle V \rangle \), \( d\langle V \rangle/dF_D \), and \( P_6 \) versus \( F_D \) for varied numbers of obstacles \( N_o \). As \( N_o \) increases, the average value of \( \langle V \rangle \) monotonically decreases, and the \( d\langle V \rangle/dF_D \) curve contains no peaks, unlike the behavior for a pinning substrate. There is a gradual decrease in \( P_6 \) with increasing \( F_D \), and there are no peaks or dips in \( P_6 \) of the type that appear for the pinning substrate. In general, we find that the obstacles produce no clear changes in the structure of the moving phase. When the number of obstacles \( N_o > 7000 \), the system undergoes plastic depinning into river-like channel flow, and remains in a uniform density, disordered flow state up to the high-
FIG. 8: (a) $\langle V \rangle$ vs $F_D$ for systems with $\phi = 0.55$ and $r_l = 300$ for varied numbers of obstacles $N_o = 2000$ to $N_o = 12000$. The inset shows the normalized cluster size $C_L$ vs the number of obstacles $N_o$ for $\phi = 0.55$ and $r_l = 300$ at $F_D = 0.0$, where there is a transition from a phase separated state at low $F_D$ to a uniform state at high $F_D$. (b) $d\langle V \rangle/dF_D$ vs $F_D$, corresponding to the system in panel (a), lacks any peak features. (c) The corresponding normalized $P_6$ vs $F_D$ has a smooth monotonic behavior. 

FIG. 9: Images of disk locations (dots) in samples with $\phi = 0.55$ and $r_l = 300$ containing obstacles consisting of fixed disks (not shown). (a) At $F_D = 0$ and $N_o = 8000$ obstacles, a disordered state appears. (b) At $F_D = 6.0$ and $N_o = 8000$, the system is still disordered. (c) $F_D = 0$ and $N_o = 2000$. (d) At $F_D = 2.0$ and $N_o = 2000$, a moving stripe state forms. 

In a recent experimental paper, Morin et al. [44] examine a colloidal flocking active matter system drifting through an obstacle array and find that when there are a large number of obstacles, the flocking behavior is lost and the flow develops riverlike properties similar to that observed in other depinning systems and resembling what we find in Fig. 1(b). In addition, Morin et al. report that there is a critical obstacle density above which the flocking behavior disappears, not unlike the cluster disappearance at high obstacle densities that we observe in Fig. 9(a). Beyond obstacle arrays, it is also possible to have active matter move over landscapes of pinning sites created via optical means, as has been demonstrated in other recent experiments [45, 46].

V. SUMMARY

We have shown that active matter assemblies driven over random pinning arrays represent a new class of system that exhibit pinning, depinning, and nonequilibrium phase transitions similar to those found for driven vortices and colloids moving over random disorder. In a regime where the system forms a phase separated state in the absence of pinning, we find that the addition of pinning causes the formation of a disordered uniform state that depins plastically into a flowing uniform state with riverlike features. At higher drives, this is followed by a transition to a moving dense stripe phase coexisting with a pinned liquid, until at the highest drives, the system transitions into a moving fully phase separated state. The different transitions are associated with features in the velocity-force and $d\langle V \rangle/dF_D$ curves that are similar to the features observed in driven non-active systems with quenched disorder. In contrast, for substrates composed of obstacle arrays, there are no dynamical transitions in the moving state and correspondingly there is a lack of features in the transport curves. At zero drive, there is a transition from a phase separated state to a
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