Collective motion of rod-shaped self-propelled particles through collision

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Self-propelled rods, which propel by themselves in the direction from the tail to the head and align nematically through collision, have been well-investigated theoretically. Various phenomena including true long-range ordered phase with the Giant number fluctuations, and the collective motion composed of many vortices were predicted using the minimal mathematical models of self-propelled rods. Using filamentous bacteria and running microtubules, we found that the predicted phenomena by the minimal models occur in the real world. This strongly indicates that there exists the unified description of self-propelled rods independent of the details of the systems. The theoretically predicted phenomena and the experimental results concerning the phenomena are reviewed.

Key words: active matter, self-propelled rods, Escherichia coli, in vitro motility assay

Emergent ordered structures in groups of motile living things such as a flock of birds [1], a school of fish [2], and cell wound healing [3] are ubiquitous. Although there is no external force and no boundary around group, living things form huge structures containing a large number of moving units through the interaction with the neighbors. Not only motile living things but motile inanimate objects such as colloids driven by electric fields [4,5] or chemical reaction [6], droplets driven by Marangoni effect [7,8], and vibrated granular rods [9,10] move in rotationally symmetric systems and the collective motions of them have been studied. One of common characteristics of animate and inanimate motile objects, so-called self-propelled particles, is that they are both “active” objects which consume free energy inside themselves or ambient environment. There are expected to be unified simple descriptions for the collective motion of both animate and inanimate active objects like the Ising model in equilibrium systems. Including the quest of the unified descriptions, nonequilibrium physics focusing on the dynamics of the structures composed of a large number of active units, which is known as active matter, is relatively new field of physics [11,12].

Active matter is classified into two types, wet active matter and dry active matter [13]. To model wet active matter like suspension of swimming bacteria in a thick cell, the momentum conservation should be considered since the flow field around bacteria is significant. In the model of dry active matter such as herds of animals on land, suspension of swimming bacteria in a thin cell, and vibrated granular particles on a plate, momentum conservation is not in general considered. The momentum is exchanged with the outside through the friction from wall. In dry active matter, head to

The investigation of collective motion of moving objects, called active matter physics, is the relatively new field of physics. One of the major studies pertaining to active matter physics is the quest for unified descriptions independent of details of systems. Although various phenomena were predicted using simple minimal models with a given symmetry, which are expected to be observed in various experimental systems, many of them had been unobserved in any experimental systems. We found in the experimental systems the various phenomena observed with the minimal models. Our results strongly indicate that there exist unified simple descriptions of the collective motion of moving objects including living objects.

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head and tail to tail alignment, called polar alignment, is permitted after collision of two motile particles. In 1995, Vicsek et al. reported the phase transition to the orientationally ordered phase in two-dimensional space governed by motility and polar alignment with neighbors using the representative agent-based model, which is called Vicsek model [14]. Using continuum model with the same symmetry as the Vicsek model, Toner and Tu reported that the phase with true long-range orientational order in two-dimensional space, which is prohibited in equilibrium systems [15], can exist [16]. In true long-range ordered phase, average of the direction of motion is the same at any place in an infinite space. This result implies that regardless of way of propulsion, self-propulsion expands the effective range of interaction, which leads to the true long-range order [17]. Due to rotational symmetry of systems, long-wavelength modes of orientation are easily excited and decay slowly. The slowly decaying fluctuations of orientation and the conservation of number of particles make bizarre density fluctuations with long-range correlation in the ordered phase [16–19]. The fluctuations can be detected as the Giant number fluctuations (GNF) [20]. Since the Vicsek model and the Toner-Tu model are minimal models with the collective motion of self-propelled particles with polar interactions, it is expected that these are the unified descriptions and the true long-range ordered phase with GNF is observed universally. The active matter having the motility and the nematic alignment to neighbors, during which one particle turn to its head or the tail of the other, was studied by Ginelli et al. [21]. In this model, all particles move at constant speed $v_0$ in two dimensions. Each particle nematically aligns to the particles within unit distance, that is, the head turns to the heads or the tails of neighbors (Fig. 1 (a)). At each time step $t$, the position of particle $j$, $r_j$, and the direction of, $\theta_j$, are updated according to

$$\theta_{j}^{t+1} = \arg\left(\sum_{k \neq j} \text{sign}(\theta_k - \theta_j)\xi_k\right) + \eta_j$$

$$r_{j}^{t+1} = r_j + v_0e^{i\theta_{j}}$$

where $k-j$ means all particles $k$ within the unit circle centered at $r_j$, and $\xi$ is a white noise uniformly distributed in $[-\pi/2, \pi/2]$. Each particle moves with a constant speed ($v_0$) when it is isolated. The first term in the upper equation leads to alignment of close particles. The noise amplitude $\eta$ and the particle density $\rho$ are the two main parameters of this model.

When $\rho=1/8$ and $v_0=1/2$, at the low $\eta$ value, the ordered phase with spatially homogeneous density was formed. The order parameter, $S(t) = \langle\exp(2\theta_j)\rangle$, was measured varying the system size, and found $S$ converged to a finite value with the increase of system size, which indicates that the nematic order was true long-range order. In other words, almost all particles aligned in parallel or in antiparallel. They measured the variance of the number of particles in a square of linear size $\ell$, $\Delta n^2$, in the case of the largest system size, $\Delta n^2$ algebraically depends on the average number in the area, $\langle n \rangle = \rho \ell^2$, as $\Delta n^2 \sim \langle n \rangle^\alpha$. If the fluctuation is normal, $\alpha$ is expected to be 0.5 from the prediction of the central limit theorem. In the homogeneous ordered phase of SPR, the estimated value of $\alpha$ is larger than 0.5, which indicates that the fluctuations with long-range correlation, called Giant number fluctuations, exist. The estimated $\alpha$ is close to the predicted value of $\alpha$ in Toner-Tu model (4/5) [16,18,19] although the symmetry of the alignment of SPR is different from Toner-Tu model. Since the model in Ref. [21] is described with only the minimal rules determined by the symmetry of self-propulsion and alignment, it is expected that the homogeneous true long-range ordered phases with GNF will be observed in various experimental systems with the same symmetry; nevertheless, there had been no experimental reports of the phase having both true long-range order and GNF until our report [25].

In the above equations, a white noise is added to the direction of motion, which means no smooth turn. In the real world, birds and fish cannot turn abruptly since rotational inertia works. Furthermore, various self-propelled particles such as *C. elegans* [27], *Mycoplasma* [28], and *E. coli* near a substrate [29] show circular trajectories. To obtain a simple description corresponding to much more kinds of active matter in the real world, we investigated the collective motion of smoothly turning self-propelled rods using the minimal agent-based model. Our model reported in [26] is

**Self-propelled rods**

A minimal discrete-time agent-based model concerning collective motion of self-propelled rods was constructed by Ginelli et al [21]. The particles in this type of active matter are called tubules driven by dyneins grafted to a glass plate [24,26]. Reported the phase transition to the orientationally ordered phase in two-dimensional space governed by motility and polar alignment with neighbors using the representative agent-based model, which is called Vicsek model [14]. Using continuum model with the same symmetry as the Vicsek model, Toner and Tu reported that the phase with true long-range orientational order in two-dimensional space, which is prohibited in equilibrium systems [15], can exist [16]. In true long-range ordered phase, average of the direction of motion is the same at any place in an infinite space. This result implies that regardless of way of propulsion, self-propulsion expands the effective range of interaction, which leads to the true long-range order [17]. Due to rotational symmetry of systems, long-wavelength modes of orientation are easily excited and decay slowly. The slowly decaying fluctuations of orientation and the conservation of number of particles make bizarre density fluctuations with long-range correlation in the ordered phase [16–19]. The fluctuations can be detected as the Giant number fluctuations (GNF) [20]. Since the Vicsek model and the Toner-Tu model are minimal models with the collective motion of self-propelled particles with polar interactions, it is expected that these are the unified descriptions and the true long-range ordered phase with GNF is observed universally. The active matter having the motility and the nematic alignment to neighbors, during which one particle turn to its head or the tail of the other, was studied by Ginelli et al. [21]. In this model, all particles move at constant speed $v_0$ in two dimensions. Each particle nematically aligns to the particles within unit distance, that is, the head turns to the heads or the tails of neighbors (Fig. 1 (a)). At each time step $t$, the position of particle $j$, $r_j$, and the direction of, $\theta_j$, are updated according to

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large vortices was observed in the region with high $\tau$ and large $\rho$ (Fig. 1(b)). At large density, spatiotemporally disordered cellular structure, an “active foam”, emerged with the middle value of $\tau$ (Fig. 1(c)). At low $\tau$ region, trains of dense traveling bands, called Vicsek waves, was observed (Fig. 1(d)). We confirmed that the smectic pattern was the asymptotic state in the subregion of the region where Vicsek waves was observed. This result means that globally polar order can emerge through purely nematic interaction, when the correlation time of rotation rate is finite.

Collective motion of elongated *E. coli*

Although there had been various experimental reports about the system with the same symmetry as SPR, no systems showed true long-range order and GNF simultaneously. Rather, disordered phases are often reported such as the chaotic phase with vortices, so-called bacterial turbulence, of suspensions of *B. subtilis* in three-dimensional space and quasi two-dimensional space [30]. This is partially due to the destabilization of order by long-range hydrodynamic interactions and too short length of objects to lead to strong alignment. For experimental verification of the prediction in [21], we avoid these two pitfalls by using filamentous non-tumbling *E. coli* in a very thin fluid layer. The filamentous *E. coli* were obtained by incubating the cells of nontumbling chemotactic mutant strain RP4979 with the antibiotic cephalixin, which inhibits cell division. The average length of...
When *E. coli* have no nematic order in a ROI, *C* is zero, and when *E. coli* are ordered more nematically in a ROI, *C* is larger. We have measured the average of *C* over both space and time for square ROIs of various areas *S*. In the disordered phases in Figure 2(a) and (b), we find that *C* ~ √*S*, as is expected in the case of finite spatial correlation length of alignment. In the ordered phase in Figure 2(d), on the other hand, a decay of *C* slower than a power law was observed. This is the signature of true long-range order. Indeed, the data is well-fitted with an algebraic approach to a finite asymptotic value of *C* – *C*∞ ~ *S*β with *C*∞ = 0.505 and β = –0.66.

To quantify number fluctuations, we binarized our images and counted the number of pixels *N*(t) covered by bacteria at time *t* varying the size of ROI. ROI was centered at the field of view. The binarization has the advantage of correcting for the slight differences in intensity resulting from variations of the height of bacteria or fluctuations in the overall light intensity. As number fluctuations, the standard deviation Δ*N* = √〈(N(t) – 〈N〉)²〉 averaged over time was calculated. In the disordered phase, we find normal fluctuations Δ*N* ~ 〈*N*〉Α with Α = 0.5. On the other hand, in the dense nematically ordered phase, Δ*N* ~ 〈*N*〉Α with Α > 0.5 i.e., GNF due to the presence of long-range correlations in the system was rigorously observed as was predicted in Ref. [21]. The estimated Α was 0.63(2) > 0.5, which is a bit smaller than the exponent estimated in [21].

Collective motion of microtubules in *in vitro* motility assay

Some of the collective motions of smoothly turning SPR...
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of curvature to be of the order of 500 μm. Since the average speed of microtubules was 8.75 μm/s, the correlation time was estimated as 61.9±0.5 s. The distribution of curvature was roughly Gaussian with the mean of –7.1×10 –4 μm –1 and the standard deviation of 1.8×10–3 μm –1.

Using high microtubule concentration (40 μg/ml), the collective motion of running microtubules was observed. On addition of ATP (at 0 min), streams along which dozens of microtubules moved in both directions were formed. The width of a stream got thicker and thicker (the upper-left figure in Fig. 4(a)), then streams started to meander (the middle and the right figures in the upper row of Fig. 4(a)). At 10–20 min, some vortices appeared (the lower row of Fig. 4(a)) and eventually covered the flow cell almost entirely (Fig. 4(b)). The shape of the vortices gradually changed over time but their diameters were almost constant, at 400 μm. It is noted that the standard deviation of curvature of isolated microtubules, which has the same order of magnitude as the average of absolute value of curvature, is of the same order as the vortex diameter. At this late stage, the vortices showed a tendency to arrange their positions into a hexagonal lattice.

Perspective

Self-propelled rods are the particles which move in the direction from the tail to the head and have short-range nematic interactions through collision, such as asymmetric reported in [26] were observed in various experimental systems. One of the examples is the hexagonal lattice of vortices of microtubules driven by dyneins grafted to a glass plate [24]. In the experiment, inner-arm dynein subspecies c (dynein c) purified from Chlamydomonas flagella was used. The dyneins fixed to a glass plate drove the microtubules whose average length was 15.6±7.3 μm. Since relatively many, randomly oriented, dyneins were attached at any time to a microtubule, smooth and isotropic motion was observed.

With low density of microtubules (0.5–1 μg/ml), the binary interactions of microtubules were analyzed. We examined 393 binary collision events. As shown in Figure 3(a) and (b), on collision, strong steric interactions occurred in the almost all events (80%), leading either to alignment or anti-alignment (70%) or to the stoppage of one microtubule (10%). 20% of the microtubules crossed each other with little effect on their trajectories. In aligning and anti-aligning collisions, the trajectory of one microtubule undergoes a sharp turn and alignment was near perfect. Thus, the outgoing angle was near 0 or π in aligning events, irrespective of the value of the incoming angle. In other words, near-perfect nematic alignment was induced by a collision. As is in the E. coli case, incoming (outgoing) angle was defined as a difference between directions of motion of two microtubules before (after) a collision.

To measure the correlation time of rotation rate of microtubules, the trajectories of isolated microtubules were analyzed using the microtubule concentration of 4.8 ng/ml. The trajectories composed of circular trajectories as is in Figure 3(c), which indicates that the rotation rate has long-time correlation, were observed. After the appropriate filtering, based on the Savitzky–Golay method [32], to eliminate the small-amplitude transverse oscillations of trajectories, we obtained the curvature as a function of distance along the trajectory and calculated its autocorrelation. Fitting the result with the exponential function, we found the persistent length of curvature to be of the order of 500 μm. Since the average speed of microtubules was 8.75 μm/s, the correlation time was estimated as 61.9±0.5 s. The distribution of curvature was roughly Gaussian with the mean of –7.1×10 –4 μm –1 and the standard deviation of 1.8×10–3 μm –1.

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Perspective

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The dependence of collective motion of *E. coli* on aspect ratio will give more knowledge about the fundamental principles governing collective behaviors of self-propelled particles, including collective motions related to biological functions such as biofilm formations and wound healing.

Unified descriptions should reproduce the dynamics of various experimental systems; therefore, inanimate self-propelled colloids with high aspect ratio will also have true long-range order and GNF. As for smoothly turning self-propelled particles, the collective motion composed of vortices like that of the microtubule were observed in the various experimental systems in various scales such as *C. elegans* (~500 μm) and motile cyanobacteria (~10 μm) (Sugi, T., Ito, H. & Nagai, K. in preparation, and Iwasaki, H., Fukasawa, Y., Kato, H., Takiguchi, M., & Nagai, K. H. in preparation). Our minimal model can reproduce the various aspects of these collective motions, therefore, our model may be the unified description of the collective motion of smoothly turning self-propelled particles.

![Figure 4](image_url)

**Figure 4** Collective motion of microtubules running on glass plate. (a) Vortex formation. Scale bar is 500 μm. (b) Lattice of vortices. Scale bar is 2 mm. Adapted from Sumino et al. (2012).
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Conflicts of interest

K. H. N. declares no competing financial interests.

Author contribution

K. H. N. contributed to review the studies of the collective motion of self-propelled rods and wrote the manuscript.

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