Renewables and Storage in Distribution Systems:
Centralized vs. Decentralized Integration
Liyan Jia and Lang Tong, Fellow, IEEE

Abstract—The problem of integrating renewables and storage into a distribution network is considered under two integration models: (i) a centralized model involving a retail utility that owns the integration as part of its portfolio of energy resources, and (ii) a decentralized model in which each consumer individually owns and operates the integration and is capable of selling surplus electricity back to the retailer in a net-metering setting.

The two integration models are analyzed using a Stackelberg game in which the utility is the leader in setting the retail price of electricity, and each consumer schedules its demand by maximizing individual consumer surplus. The solution of the Stackelberg game defines the Pareto front that characterizes fundamental tradeoffs between retail profit of the utility and consumer surplus.

It is shown that, for both integration models, the centralized integration uniformly improves retail profit. As the level of integration increases, the proportion of benefits goes to the consumers increases. In contrast, the consumer-based decentralized integration improves consumer surplus at the expense of retail profit of the utility. For a profit regulated utility, the consumer-based integration may lead to smaller consumer surplus than that when no renewable or storage is integrated at either the consumer or the retailer end.

Index Terms—Distributed energy resources, microgrid, renewable integration home energy storage, dynamic pricing, game theory in demand response.

I. INTRODUCTION

The power grid is facing an imminent transformation, perhaps one of the most profound in its 130 years history. This transformation is brought by disruptive innovations that challenge basic premises that governs its design and operation.

One of the premises is the long-held axiom that the operation of the grid is governed by the law of instantaneous balance of generation and consumption. Thus the principle of operation is to forecast demand accurately, secure inexpensive generation resources, and procure sufficient reserves to cope with uncertainties. The resulting approaches, unfortunately, often result in complex, ad hoc, and costly practices. Indeed, the requirement of instantaneous power balance is one of the fundamental barriers to integrating a high level of intermittent renewables that defy accurate forecast.

The axiom of instantaneous power balance is challenged by the recent introduction of commercial grade batteries for home energy storage. The possibility that energy storage is omnipresent in the power grid has profound implications: demand no longer needs to be balanced instantaneously and volatilities due to renewables drastically smoothed out. A relevant point of reference is the role of buffer in the Internet. It is precisely the omnipresence of such memory elements throughout the Internet that makes it possible to stream high definition video in real-time over unreliable and stochastic networking environments.

The other premise called into question is the notion that the transmission grid is the central artery that delivers power from generation sites to millions of end users. The architecture of power delivery is a unidirectional transfer of power from generators through transmission networks to distribution networks and to consumers. Such an operation paradigm requires over provisioning of generation and transmission capacities to ensure that extreme demands are met under contingencies. The cost of over-provision, however, is enormous. The difference between the high and the low hourly prices over the course of a typical year can be up to four orders of magnitude.

The premise of unidirectional power delivery is also challenged by the phenomenal growth in photovoltaic (PV) installations at the consumer end, driven by the precipitous drop of PV cost and policies that promotes clean energy. A key policy is the widely adopted net-metering mechanism that effectively allows the consumer to sell back locally generated surplus energy at the retail price. As a result, power generated at the consumer end becomes a potential source of overall power supply, resulting in a new paradigm of power delivery based on a bidirectional model where a substantial part of the power generation may come from the consumer end.

The transformative innovations of large scale PV and storage present new engineering and social economic challenges. At the core of these challenges is the complex question on how large scale renewables and storage are integrated into the overall power delivery. Answers to such questions have significant impacts on architectures of control, communications, and markets for the future power grid.

A. The Death Spiral Hypothesis and Integration Models

The rise of renewable integration by consumers has led to the so-called death spiral hypothesis for retail utilities [2], [3]: the decline of consumption due to below-the-meter renewable generation by consumers triggers an upward pressure on the rate of electricity and threatens the economic viability of the retail utility. As a regulated monopoly, the retail utility ultimately has to raise the rate of electricity, which acceler-
ates consumer adoptions of distributed generation that further erodes the revenue of the utility.

Alternative rate structures have already been proposed that makes connection charges a more significant part of the cost for the consumers. Such increases erect a seemingly artificial barrier that inhibits renewable integration. If implemented indiscriminately, it shifts the cost to those without the capability of below-the-meter renewable generation.

Insights into the death spiral hypothesis can be gained by a better understanding of integration models in distribution systems. To this end, we consider two types of integrations; one is the below-the-meter integration by consumers, the other is the above-the-meter integration by the utility.

For the utility-based integration, the utility owns the integration resource. The operation decisions are centralized with a global objective, unobservable to the consumers. The integrator can coordinate resources within its service area, mitigating uncertainties inherent in renewable integration. We thus refer this model to as centralized integration.

For the consumer-based integration, consumers own the energy resources and operate the integration and storage devices. The integration is therefore decentralized driven by individual objectives of consumers. In this case, renewable integration and storage operations are below the meter, unobservable to the retail utility. We call this model decentralized integration.

It is intuitive that decentralized integration may have adverse effect on the revenue of the utility. Does it benefit consumers? The answer may be less obvious and more nuanced. To a consumer who still relies on the grid to deliver power at times of shortage, it is not clear whether the benefit of locally generated renewables offsets the cost increase of electricity purchased from the retailer. For the centralized integration, it is not clear whether the utility will share the derived benefit with consumers such that consumers find it economically attractive to stay with the utility’s integration model rather than switching to the consumer-based integration; the latter creates a drift toward the death spiral.

B. Related work

The literature on renewable integration and storage in distribution systems is broad and extensive. Here we highlight some of the relevant literature that focuses on interactions between consumers and a distribution utility in the presence of renewable generation and storage in distribution systems. Hereafter, we use the terms distribution utility and retailer interchangeably as we consider the retail functionality of the distribution utility.

Our discussion centers around three broad areas: (i) retail pricing of electricity; (ii) consumer-retailer interaction with renewable integration; (iii) consumer-retailer interaction with storage integration.

1) Retail Pricing and Real-time Price (RTP): The interaction between the retailer and consumers is fundamentally defined through the pricing of consumption. For consumer participation in a smart grid, pricing of electricity that reflects the overall system demand and supply plays a central role. To this end, the notion of real-time pricing (RTP) has received considerable attention since the deregulation of electricity market. RTP allows the price of electricity to vary with time, and it has been widely argued that RTP is critical for an efficient electricity market [4]. It was pointed out in [5] that RTP brings significant gain in efficiency even if “demand shows very little elasticity.” When renewable generation is considered, studies show that RTP can increase the percentage of load served by renewables even when the demand has low elasticity [6].

In this paper, we consider a special form of RTP referred to as day ahead hourly pricing (DAHP). DAHP sets the price of electricity for retail consumers one day ahead, possibly in conjunction with the clearing process of the day ahead wholesale market. The rationale is that DAHP provides a level of price certainty that allows a consumer to plan her consumption accordingly. It also avoids potential volatility and instability when RTP is determined based on the real-time locational marginal prices (LMP) [7]. DAHP has been implemented by several utility companies in the U.S. [8].

It is natural to model consumer-retailer interaction in a game theoretic setting; the retailer sets the price of electricity and the consumer adjusts the consumption accordingly. This is the Stackelberg game model adopted in this paper and it has been used earlier. In particular, the authors of [9] used the Stackelberg game to develop an adaptive pricing scheme that maximizes social welfare. The work of Chen et al. [10] and Li et al. [11] considered the problem of setting retail price of electricity via distributed social welfare optimization and equilibrium analysis. These results characterize consumer-retailer interaction under the setting of social welfare maximization. They are not adequate for analyzing the consumer-retailer interaction when their interests are not well aligned.

2) Consumer-retailer interaction with renewable integration: Renewable integration in distribution systems has profound implications on consumer-retailer interactions; the death spiral hypothesis discussed earlier is one such example. The first study of the death spiral hypothesis is by Cai et al. [2]. The empirical study is based on a model that captures the closed loop dynamics of consumer adoption (at the yearly time scale). The cost of net-metering and the effect of connection charge are also considered.

A relevant line of work is pricing of electricity in the presence of renewables. The authors of [12] considered the problem of contract design between renewable generators and energy aggregators who are responsible for a large scale PHEV charging. The work in [12] shows that, by coupling with deferrable loads, the costs resulting from stochastic generation can be significantly mitigated. In [13], [14], a stochastic optimization framework for retail pricing is formulated that takes into account uncertainty associated with the wholesale market and the uncertainty associated with consumer demand.

3) Consumer-retailer interaction with storage integration: There has been broad interest in the role of storage in distribution networks, especially when it is coupled with the charging of electric vehicles. The existing literature focuses

*Here we use utility to include distribution utility as well as energy aggregators.
†The utility may also contract renewable providers and storage operators.
mostly on the optimal management of storage usage and the economic benefits of storage. A particularly relevant work is [16] where the authors pointed out that the presence of storage may result in gains in consumer surplus, losses in generator surpluses, and net welfare gain. Incentives for storage usage by the merchant storage operators, generators, and consumers and structures of storage ownership are analyzed in [17].

There has been a considerable amount of work on optimal storage management under various settings. See [18] and references therein. The problem is in some way similar to the inventory control problem but has special characteristics unique to the distribution and consumption of electricity. In particular, a threshold structure of the optimal policy of storage operation is obtained and analyzed in [13]. Similar results are also obtained in [19] under more general pricing and demand models. The authors of [20] considered the interesting problem of cooperative or competitive operations between storage and renewable generations. These existing results, however, do not address directly the impact of storage on consumer-retailer interactions, which is the main focus of the current paper.

C. Summary of results and notations

This paper focuses on how economic benefits of renewable and storage integration are distributed between the utility and the consumers, and how different integration models affect such distributions. The analytical framework presented here was first proposed in [21] and further developed in [22]. The application of this framework to renewable integration was first presented in a conference version of the paper [23] and with additional material added here. The analysis and numerical results of storage integration under two integration models are new.

Standard notations are used throughout the paper. We use \( x^+ \) to represent \( \max\{0, x\} \), and \( x^- \) to represent \( \max\{0, -x\} \). For a vector \( x \), \( x^T \) is its transpose. Here \( x = (x_1, \ldots, x_N) \) is for a column vector and \( [x_1, \ldots, x_M] \) for a row vector. For a random variable \( x \), \( \mathbb{E}(x) \) is the expected value.

II. SYSTEM MODEL

We assume that the retail utility participates in a two-settlement wholesale market as a load serving entity; it submits bids in the day ahead market that sets the day ahead price, and it is a price taker in the real-time market. The retailer determines the day ahead hourly price (DAHP) and makes it available to the consumer. The consumer adjusts its consumption in real time.

A. Dynamic Pricing

DAHP is defined a 24 dimensional vector \( \pi \) posted one day ahead and fixed throughout the day of operation; it is a generalization of some of the existing pricing schemes: the uniform pricing is when entries of \( \pi \) are the same; the critical peak pricing (CPP) and the time of use (TOU) pricing is when entries of \( \pi \) corresponding to the peak hours are different from those in off-peak hours. The retailer can also index DAHP to the day ahead prices at the wholesale market. In this paper, we are interested in optimized DAHP by the retailer under a general notion of social welfare.

B. Consumer Surplus and Optimal Demand Response

The benefit to consumer is measured by the consumer surplus (CS) defined by the utility of consumption minus the cost. We are interested in characterizing the demand function associated the optimal demand response to DAHP. To this end, we consider a linear demand model (Theorem 1) that arises from the thermostatically controlled load (TCL) where the energy state (temperature) is controlled by thermostatic controlled heating-ventilation and air conditioning (HVAC) units.

Empirical study [24] shows that temperature evolution can be modeled by a discrete-time dynamic equation given by

\[
\begin{align*}
 x_t &= x_{t-1} + \alpha (a_t - x_{t-1}) - \beta p_t + w_t, \\
 y_t &= (x_t, a_t) + v_t,
\end{align*}
\]

where \( x_t \) is the indoor energy state (temperature), \( a_t \) the outdoor temperature, \( p_t \) the power drawn by the HVAC unit, \( y_t \) the temperature measurement, \( w_t \) and \( v_t \) the process and measurement noise, respectively, that are assumed to be zero mean and Gaussian.

System parameters \( \alpha \in (0, 1) \) and \( \beta \) model the insolation of the building and efficiency of the HVAC unit. The above equation applies to both heating and cooling scenarios. But we exclude the scenario that the HVAC does both heating and cooling during the same day, focusing herein on the cooling scenario (\( \beta > 0 \)) without loss of generality.

Assuming that a consumer’s discomfort level can be measured by the squared deviation of energy state from her preferred setting, the CS for consumer \( k \) over a period of \( N \) intervals is given by

\[
\text{CS}^{(k)}(\pi) = -\mu^{(k)} \sum_{t=1}^{N} (x_t^{(k)} - \theta_t^{(k)})^2 - \pi^T p^{(k)}, \tag{2}
\]

where \( \pi \) is the DAHP vector, \( p^{(k)} \) the vector of power usage over \( N \) periods, \( x_t^{(k)} \) and \( \theta_t^{(k)} \) are the actual and desired energy states, respectively, in interval \( t \), and \( \mu^{(k)} \) a coefficient that converts the level of discomfort to some monetary value.

Note that \( \pi \) should contain prices at the same time scale as the system dynamics (by duplicating hourly prices). To simplify notation, we assume that the time \( t \) is at the hourly scale. The results here can be generalized easily. See [22]. Note also that CS defined here is always negative. It represents the total equivalent cost (actual cost plus the cost converted from discomfort level) each consumer needs to pay over \( N \) periods.

Given DAHP \( \pi \), the optimal demand response for consumer \( k \) is to maximize its expected CS with respect to the random noises \( w \) and \( v \),

\[
\max_{\mu^{(k)}} \mathbb{E} \left\{ -\mu^{(k)} \sum_{t=1}^{N} (x_t^{(k)} - \theta_t^{(k)})^2 - \pi^T p^{(k)} \right\},
\]

s.t. \( x_t^{(k)} = x_{t-1}^{(k)} + \alpha (a_t - x_{t-1}^{(k)}) - \beta p_t^{(k)} + w_t^{(k)}, \)

\[
y_t^{(k)} = (x_t^{(k)}, a_t) + v_t^{(k)},
\]

where the expectation is taken over the observation and process noises. Here we ignore the positivity constraint on \( p^{(k)} \), and assume that the resulting optimal power consumption is positive. This assumption is reasonable when the DAHP doesn’t vary too much during a day and \( \mu \) is large. The
following theorem gives the aggregated demand function and
the consumer surplus summed over all consumers.

Theorem 1 (Optimal Demand Response [22]): Assume
that the process noise is Gaussian with zero mean for all
consumers. Given DAHP $\pi$, the optimal aggregated residential
real-time demand and the expected total CS are given by, respectively,

\[
ed^{RT}(\pi) = \sum_k p^{(k)} = b - G\pi, \quad (4)
\]
\[
\text{CS}(\pi) = \pi^T G \pi/2 - \pi^T b + c, \quad (5)
\]

where matrix $G \geq 0$ is deterministic and positive semi-
definite, and it depends only on system parameters and user
preferences. Parameter $b$ is a Gaussian vector independent of
$\pi$, and $c$ is a deterministic constant, also independent of $\pi$.

Hereafter, our analysis is based on the optimal demand
response of the form in (4) and independent of how (4) arises
from the types of demand response applications.

C. Retail Profit

The retail profit (RP) for the utility is the difference between
the revenue from its customers and the cost of power. Let
$\lambda = (\lambda_1, \lambda_2, ..., \lambda_T)$ be the random vector of wholesale spot
prices of electricity at times of consumption, which represents
the marginal cost of procuring electricity from the wholesale
market. In absence of renewables accessible to the retailer, the
retail profit $\pi_r(\pi)$ is given by

\[
\pi_r(\pi) = (\pi - \lambda)^T d^{RT}, \quad (6)
\]

where $d^{RT}$ and $\lambda$ are random and $\pi$ the decision variable
representing the utility’s action.

As a load serving entity, the utility takes into consideration
its own profit and consumers’ satisfaction. Here we define the
weighted expected social welfare as

\[
\overline{\text{sw}}_\eta(\pi) = \overline{\pi_r(\pi)} + \eta \text{CS}(\pi), \quad (7)
\]

where the expectation is taken over randomness in the real
time wholesale price of electricity $\lambda$ and the randomness in
the consumer demand in (4). When $\eta = 0$, (7) corresponds
to the profit maximization and $\eta = 1$ the social-welfare
maximization.

III. A STACKELBERG GAME MODEL AND ITS SOLUTION

It is natural to model utility-consumer interaction via DAHP
by a Stackelberg game where the utility is the leader and the
consumers are the followers; the action of the leader is to set DAHP $\pi$ one day ahead, and followers respond with real
time consumption. The payoffs for the consumer is $\text{CS}(\pi)$, and
payoff to the utility is $\overline{\text{sw}}_\eta(\pi)$.

For a fixed $\eta$, the Stackelberg equilibrium is obtained
via backward induction in which the optimal response of a
follower is given in Theorem1 and the optimal action of the
leader is to set DAHP optimally by

\[
\pi^*(\eta) = \arg \max \{\pi_r(\pi) + \eta \text{CS}(\pi)\}. \quad (8)
\]

Fig. 1: CS-RP trade-offs without integration and the Pareto
front. The point associated $\pi^w$ is the social welfare optimal tradeoff, $\pi^r$ the profit maximizing tradeoff, and $\pi^w$ the profit regulated tradeoff associated with retail profit $\Delta$.

By varying $\eta$, we obtain the Pareto front of CS-RP tradeoffs
defined by

\[
\mathcal{P} = \left\{ (\text{CS}(\pi^*(\eta)), \overline{\pi_r(\pi^*(\eta))}) : \eta \in [0, 1] \right\}, \quad (9)
\]

where each point on the Pareto front represents an optimal CS
vs. RP tradeoff associated with an optimal DAHP $\pi^*(\eta)$ as a
solution of (8). As a function of $\pi$, the weighted social welfare
is given by

\[
\overline{\text{sw}}_\eta(\pi) = \frac{\eta}{2} \pi^T G \pi + \pi^T (1 - \eta) b + G \lambda + \eta c, \quad (10)
\]

from which we obtain the optimal DAHP as

\[
\pi^*(\eta) = \frac{1}{2 - \eta} \lambda + \frac{1 - \eta}{2 - \eta} G^{-1} b, \quad (11)
\]

where the first term depends only on the expected wholesale
price of electricity $\lambda$. This term shows that the optimal DAHP
follows the average wholesale price. The second term depends
only on the consumer preference and randomness associated
with consumer environments.

Fig.1 illustrates various CS-RP tradeoffs. The shaded area
represents the achievable region of CS-RP pairs by suitably choices of DAHP, and the boundary of the shaded regions is
the Pareto front of all valid tradeoffs.

Various properties of the achievable region of the CS-
RP tradeoff have been established in [22]. In particular, the
achievable region is convex, and Pareto front concave and
decreasing. A particularly important point on the Pareto front
represents the social welfare optimizing pricing $\pi^w$. It has been shown that $\pi^w = \lambda$, and the resulting retail profit
is zero [22], which implies that the social-welfare maximizing
objective is not economically viable for the utility. If the utility
has to operate at some level of retail profit $\Delta$ as a regulated
monopoly, it is to the utility’s interest to maximize consumer
surplus by setting DAHP at $\pi^r$.

IV. RENEWABLE INTEGRATION

In this section, we discuss how renewable integration
changes the characteristics of the Pareto front of the CS-RP
tradeoff under the centralized and decentralized integration
models. We first provide intuitions of these results followed
by detailed analysis.

For the simulations in this section, we used the actual
weather record in Hartford, CT, from July 1st, 2012 to
July 30th, 2012. The day-head price (used as prediction) and
real-time price (used as realization) were also for the same
period from ISO New England. The HVAC parameters for
the simulation was set as: \( \alpha = 0.5, \beta = 0.1, \mu = 0.5 \).
The desired indoor temperature was set to be 18°C for all hours. The size
of total consumers is 1000.

A. General characteristics and intuitions

A graphical sketch of the main results is shown in Fig. 2
where the left panel compares the Pareto fronts with and
without renewables under the centralized integration, and the
right panel is the comparison under decentralized integration.

a) Centralized integration: For the centralized integration,
as expected, the Pareto front is strictly above that of no
renewable integration, as shown in Fig. 2(a). Note that if the
utility operates at a fixed retail price as a regulated monopoly,
renewable integration by the utility results in increased con-
sumer surplus.

Our result further quantifies the distribution of benefits
among the utility and the consumers. In particular, we show
in Theorem 2 that the benefit of renewables goes to the con-
sumers only if the available renewable capacity \( K \) exceeds a
certain threshold. As \( K \) increases, the benefits from renewable
integration apportioned to consumer increases monotonically.

The intuition behind the threshold behavior is as follows.
When the amount of renewables is small, the utility simply
uses the available renewables to reduce the amount of pur-
chased power from the grid. In this regime, the Pareto front
shifts straightly upward, which means that all benefits go to
the utility. As the amount of renewable increases, it becomes
necessary that the utility reduces the retail price to stimulate
consumption. Therefore, beyond the threshold, the Pareto front
shifts upright; the utility and the consumer split the profit.

b) Decentralized integration: For the consumer-based
integration, we show in Theorem 3 that the Pareto front with
renewable integration intersects with that when there is no
renewable integration, as illustrated in Fig. 2(b). The intuition
for this behavior comes from examining the points on the
Pareto front corresponding to the social welfare maximizing
price and the retail profit maximizing price.

Consider first the retail profit maximizing point on the
Pareto front. Because the renewable integration is below the
meter, the retailer simply experiences the reduced consump-
tion, and the maximum retail profit decreases. For the social
welfare maximizing point, because the retail profit is zero,
the renewable integration benefits entirely to the consumer.
We thus expect that the new social welfare optimizing price
results in increased consumer surplus. Interpolating the two
points, the corresponding Pareto front must intersect with that
when there is no renewable.

The case of profit regulated utility is particularly interesting.
Depending on the level of regulated retail profit, decentralized
renewable integration by the consumer may lead to reduced
consumer surplus as illustrated in Fig. 2(b). The reason is
that, the renewable integration below the meter reduces the
consumption, which forces the utility to increase the retail
price to cover the loss of revenue. If the energy cost increase
is greater than the utility of consumption, the consumer surplus
is reduced.

B. Analysis of Centralized Renewable Integration

We now analyze the Pareto front when the utility owns and
operates centrally renewable integration. We assume that the
amount of renewable is not large enough to satisfy all demand
of its service area, or equivalently, any excess of renewable is
spilled.

For simplicity, we assume zero cost of using renewable
energy and denote the renewable available for the retailer in
each hour as a random vector \( q = (q_1, ..., q_24) \). The retail
profit after renewable integration then becomes

\[
\rho^r(\pi) = \pi^r d^{ret} - \lambda^r (d^{ret} - q)^+. 
\]

(12)

The CS-RP region achievable by DAHP will be enlarged by
renewable integration, obviously. What is less obvious is to
what degree renewable benefits consumers. If the Pareto front
in Fig. 2(a) moves straight upwards, then the utility captures all
the benefit. If the Pareto front shifts up right, both the utility
and the consumer benefit at perhaps different degrees.

The following theorem characterizes how the benefits are
distributed between the utility and the consumers for deter-
ministic demand function.

**Theorem 2 (Centralized Renewable Integration):** Assume
that \( q_i \) are independently distributed over \([0, KT]\) and
the demand function associated with the optimal demand
response is deterministic \((b = b)\). Let \( \Delta \rho^r(\eta) \) and \( \Delta \bar{C}S(\eta) \)
be the increase of retail profit and consumer surplus due to
renewable integration for fixed \( \eta \), respectively. Then,

1) for all \( \eta \), \( \Delta \rho^r(\eta) > 0 \).
2) There exists a \( \tau \) such that the consumer surplus improves
only when \( K > \tau \). Specifically, \( \Delta \bar{C}S(\eta) = 0 \) for \( K \leq \tau \)
and \( \Delta \bar{C}S(\eta) > 0 \) otherwise.
3) The fraction of renewable integration benefit to the
consumers \( \frac{\Delta \bar{C}S(\eta)}{\Delta \rho^r(\eta)} \rightarrow \frac{1}{3-2b} \) as \( K \rightarrow \infty \).

**Proof:** Without renewable integration, for a particular \( \eta \),
the first order condition of Eq. (8) gives that the optimal price
\( \pi^*(\eta) \) satisfies

\[
(\eta - 2)G \pi^*(\eta) + (1 - \eta)\tilde{b} + G\lambda = 0.
\]
Since optimal demand level satisfies \( \bar{d}(\eta) = \bar{b} - G\pi(\eta) \), the previous condition is equivalent to

\[ \bar{b} - (2 - \eta)\bar{d}(\eta) = G\lambda. \]

With renewable integration, the utility optimizes

\[
\bar{\pi}_s(\pi) = \pi^T(d - \lambda^T b) + \eta(\pi^T G\pi/2 - \pi^T \bar{b} + c)
\]

\[ = \bar{b}^T G^{-1}d - \bar{d}^T G^{-1}d - \sum_i \lambda_i \int_0^{\bar{d}_i} (\bar{d}_i - q_i) f_i(q_i) dq_i + \eta(\bar{d}^T G^{-1}d/2 - \bar{G}^{-1}b/2 + c) \]

(13)

where \( \bar{d} = \bar{b} - G\pi \) and \( f(q) = (f_1(q_1), ..., f_{24}(q_{24})) \) is the marginal PDF of the renewables. We can have the first order condition with respect to the optimal demand level \( \bar{d}_r(\eta) \), which satisfies

\[ \bar{b} - (2 - \eta)\bar{d}_r(\eta) = G(\lambda \circ F(\bar{d}_r(\eta))), \]

where \( \circ \) means the Hadamard product, i.e., piecewise product of two vectors. \( F = (F_1, ..., F_{24}) \), where \( F_i \) is the marginal cdf of renewable energy’s distribution at hour \( i \).

If for all \( i \), \( KT_i \leq \bar{d}_r(\eta) \), \( F_i(\bar{d}_r(\eta)) = 1 \), we can see that \( \bar{d}(\eta) \) satisfies the optimal condition (14). Therefore \( \bar{d}_r(\eta) = \bar{d}(\eta) \), \( \pi_r(\eta) = \pi(\eta) \), the change of consumer surplus \( \Delta cs(\eta) = 0 \). Otherwise, if for some \( i \), \( KT_i > \bar{d}_r(\eta) \), \( F_i(\bar{d}_r(\eta)) < 1 \). Therefore \( \bar{d}(\eta) \) does not satisfy the optimal condition (14). Denote \( \bar{d}_r(\eta) = \bar{d}(\eta) + G\delta/(2 - \eta) \), where \( \delta = \lambda - \lambda \circ F(\bar{d}_r(\eta)) \geq 0 \). Then,

\[ \Delta cs(\eta) = \frac{1}{2}(\{\bar{d}_r(\eta)\}^T G^{-1} \bar{d}_r(\eta) - \{\bar{d}(\eta)\}^T G^{-1} \bar{d}(\eta))
\]

\[ = \frac{1}{\pi} \{2\delta^T \bar{d}(\eta) + \delta^T G\delta \} > 0. \]

For the retail profit, for all \( K \) and \( \eta \),

\[ \Delta \bar{\pi}_s(\eta) = (\pi^T(\eta)\bar{d}_r(\eta) - \lambda^T \bar{d}_r(\eta) - q^+ + \pi^T(\eta)\bar{d}_r(\eta) - \lambda^T \bar{d}_r(\eta) - \pi^T(\eta)\bar{d}_r(\eta) - \lambda^T \bar{d}_r(\eta) - \{\bar{d}_r(\eta)\}^T G^{-1} \bar{\bar{d}}_r(\eta))
\]

\[ + \frac{1}{\lambda^T \bar{\bar{d}}_r(\eta)} \{\{d_r(\eta)\}^T G^{-1} \bar{d}_r(\eta) - (d(\eta)) \}^T G^{-1} \bar{d}(\eta)) \] ≥ 0,

where \( \bar{\lambda} = \text{diag}(\lambda_1/\Gamma_1, ..., \lambda_{24}/\Gamma_{24}) \). As \( K \) goes to infinity, \( \bar{d}_r(\eta) \) is bounded, \( \Delta \bar{\pi}_s(\eta) \) goes to \( (1 - \eta)\{\{d_r(\eta)\}^T G^{-1} \bar{d}_r(\eta) - \{d\eta\} \}^T G^{-1} \bar{d}(\eta) \}, \Delta cs(\eta) \) equals to \( \frac{1}{\pi} \{\{d_r(\eta)\}^T G^{-1} \bar{d}_r(\eta) - (d(\eta)) \}^T G^{-1} \bar{d}(\eta) \}, \) then

\[ \frac{\Delta cs(\eta)}{\Delta \bar{\pi}_s(\eta)} \] goes to \( \frac{1}{3 - 2\eta} \).
With the increase of renewable energy level, we can see that the maximized retail profit decreases, which means that utility-based renewable brings more benefit completely outside the one with consumer-based integration, moves to the right along the original trade-off curve.

Since \( \bar{\lambda}^1 \bar{s} > 0 \), the social welfare maximization point, \((0, \bar{SW}_s(\bar{\lambda}))\), is outside the original CS-RP trade-off curve without renewable energy. As \( \bar{s} \) increases, the maximized social welfare also increases.

When \( \eta = 0 \), the payoff function is the retail profit, \( \bar{\rho}_s(\pi) = (\pi - \bar{\lambda})^T(\bar{b} - \bar{s} - G\pi) \). Therefore, the optimal price is \( \pi_s^* = \frac{1}{2}(G^{-1}\bar{b} - G^{-1}\bar{s} + \bar{\lambda}) \). The retail profit change with renewable energy is,

\[
\Delta \bar{\rho}_s = \bar{\rho}_s(\pi^*) - \bar{\rho}_s(\pi_s^*) = -\frac{1}{2}(G^{-1}\bar{b} - \lambda)^T\bar{s}.
\]

Since \( G^{-1}\bar{b} \) is the price to make demand equal to zero, \( G^{-1}\bar{b} - \lambda \geq 0 \). Therefore, \( \Delta \bar{\rho}_s < 0 \). The maximized profit decreases. Also, we can see that the maximized retail profit decreases with the increase of renewable energy level \( \bar{s} \).

Fig. 5 shows numerical results under different integration levels of renewable. It is apparent that the Pareto fronts at 1MW and 3MW have crossovers with the that associated with no renewable integration. It is also evident that, as the level of renewables increases, the maximized retail profit decreases, the maximized social welfare increases, and the cross point moves to the right along the original trade-off curve.

We also compared distributed and centralized control of renewable energy with the same level of integration. As shown in Fig. 6, the tradeoff curve with utility-based renewable is completely outside the one with consumer-based integration, which means that utility-based renewable brings more benefit to the retail market, in absence of other considerations.

Fig. 6 shows numerical results under different integration levels of renewable. It is apparent that the Pareto fronts at 1MW and 3MW have crossovers with the that associated with no renewable integration. It is also evident that, as the level of renewables increases, the maximized retail profit decreases, the maximized social welfare increases, and the cross point moves to the right along the original trade-off curve.

We now consider storage integration under the centralized and decentralized integration models. The problem and the technique of analysis are similar to that used in renewable integration except that we need to obtain the optimal policy of storage operation.

For the simulations in this section, we used the same basic setup as Section IV. For storage, we set the storage size as 10KW for individual houses, initial storage level as 0, all efficiency coefficient as 0.95 and ramp limit as 5KW.

A. General characteristics and intuitions

As we will show in the following two subsections, the characteristics of centralized and decentralized models for storage, as shown in Fig. 7, are similar to renewable integration.

For the centralized model, the CS-RP tradeoff region is enlarged as shown in Fig 7(a). Different from the case in renewable integration, the Pareto front is shifted strictly up, indicating that the benefit of storage goes entirely to the utility.

This is due to the fact that, under centralized integration, the optimal use of storage by the utility is to arbitrage electricity in the wholesale market, independent of consumer response. The gain from storage integration all goes to the utility.

For the decentralized integration, as in Fig 7(b), under some conditions (as shown in Theorem 3), the tradeoff curve intersects with the original one, similar to the case of decentralized integration of renewables. The reasons behind this is somewhat different from those in renewable integration, although the method of analysis is similar. Since the consumers have the ability to shift their energy usage, they can reduce the payment by charging during the low price hours and discharging during the high price hours. Therefore the maximized retail profit is decreased. On the other hand, in the social welfare maximization case, the utility passes the distribution cost to the consumers. In this case, the storage is used to arbitrage over the cost to increase the social welfare. Therefore, the new tradeoff curve intersects with the previous one.

B. Analysis of Centralized Storage Integration

Denote the storage level at hour \( i \) as \( B_i \), and the energy charged into the storage as \( r_i \) (when \( r_i \leq 0 \), it means discharging the storage). To differentiate charging and discharging scenarios, we use \( r^+ \) to represent the positive
and negative part of \( r_t \), i.e., \( r_t = r^+_t - r^-_t \), respectively. The dynamics of the battery can be expressed as

\[
B_{t+1} = \kappa(B_t + \tau r^+_t - r^-_t / \rho),
\]

where \( \kappa \in (0, 1) \) is the storage efficiency, \( \tau \in (0, 1) \) the charging efficiency, and \( \rho \in (0, 1) \) the discharging efficiency.

Retail profit of the utility is the difference between revenue and cost. For revenue, centralized storage integration does not affect the optimal demand response by consumers. Therefore, for fixed DAHP \( \pi \), the revenue for the utility is the same with or without storage integration. On the other hand, storage integration allows the utility arbitrage over the wholesale price to reduce cost, thus increasing the overall retail profit. Formally, the retail profit with centralized storage integration, \( \pi \), can be expressed as

\[
\pi_c = \max_{r^+, r^-} \pi^T d - \lambda^T (d + \tau r^+ - r^-) - \psi^T r^+ - \psi^T r^- - \rho r^- / \rho,
\]

\[
s.t. \quad B_{t+1} = \kappa(B_t + \tau r^+_t - r^-_t / \rho), \quad B_{24} = B_0, 0 \leq B_i \leq C, \quad 0 \leq r^+_t \leq r^u, 0 \leq r^-_t \leq r^d,
\]

where \( \psi^+ \) and \( \psi^- \) are the costs associated with charging and discharging the battery, \( B_0 \) the initial energy level in the storage, \( C \) the capacity of the battery, \( r^u \) the charging limit, and \( r^d \) the discharging limit.

Notice that both the objectives and constraints can be separated for the part with price \( \pi \) and the part with storage control policy \( r \), the retail profit with centralized storage, \( \pi_c \), can be expressed as sum of the original retail profit, \( \pi \), and the arbitrage profit \( Q(\lambda) \), i.e., \( \pi_c = \pi + Q(\lambda) \), where \( Q \) is defined as.

\[
Q(\lambda) = \max_{r^+, r^-} \pi^T d - \lambda^T (d + \tau r^+ - r^-) - \psi^T r^+ - \psi^T r^- - \rho r^- / \rho,
\]

\[
s.t. \quad B_{t+1} = \kappa(B_t + \tau r^+_t - r^-_t / \rho), \quad B_{24} = B_0, 0 \leq B_i \leq C, \quad 0 \leq r^+_t \leq r^u, 0 \leq r^-_t \leq r^d.
\]

Since zero vector is a feasible solution, we have \( Q(\lambda) \geq 0 \).

With the preference weight parameter on consumer surplus \( \eta \), the retailer’s payoff function is

\[
\pi_c(\pi) + \eta CS(\pi) = \pi(\pi) + \eta CS(\pi) + Q(\lambda).
\]

Therefore, for any \( \eta \), the optimal price for the retailer is the same as in the case without storage, and the Pareto front is shifted up by \( Q(\lambda) \).

### C. Analysis of Decentralized Storage Integration

We now consider decentralized storage integration by consumers. With storage and known DAHP, a consumer can optimize charging and discharging decisions. We assume that consumers have the net-metering option that allows them to sell back surplus energy stored in the battery. But we restrict to the case that the storage capacity is below the level of aggregated demand, so that the retail price will always be positive. We believe that this assumption is reasonable at current storage integration level.

Using the same notation for storage as in Section V-B, the optimal demand response problem for the consumers with decentralized storage is changed to

\[
\max_{\pi, r^+, r^-} \mathbb{E}_{w, r} \left\{ -\mu \sum_{t=1}^{T} (x_t - \theta_t)^2 - \pi^T (p + r^+ - r^-) - \psi^T r^+ - \psi^T r^- - \rho r^- / \rho \right\}
\]

\[
s.t. \quad x_t = x_{t-1} + \alpha (a_t - x_{t-1}) - \beta p_t + w_t,
\]

\[
y_t = (x_t, a_t) + v_t,
\]

\[
B_{t+1} = \kappa(B_t + \tau r^+_t - r^-_t / \rho),
\]

\[
B_{24} = B_0, 0 \leq B_i \leq C,
\]

\[
0 \leq r^+_t \leq r^u, 0 \leq r^-_t \leq r^d.
\]

Under the net-metering assumption (see [19] for more general results), the above optimization can be divided into two independent sub problems: optimizing demand response as if storage does not exist and optimizing storage for arbitrage as if there is no demand. This means that adding storage on the demand side doesn’t change the original linear relationship between the actual energy consumption and retail price; the benefit of storage to the consumer side is in the form of arbitrage options.

Given the retail price \( \pi \), let \( r(\pi) \) be the optimal charging vector by solving an equivalent of (17) and obtain \( Q(\pi) \). With decentralized storage integration, the consumer surplus is changed to \( \pi_{cs}(\pi) = \sum_{t=1}^{T} r_t \) and the retail profit with consumer-based storage is \( \pi_{rb}(\pi) = \pi(\pi) + \pi^T r(\pi) - \lambda^T r(\pi) \).

By varying \( \eta \in [0, 1] \), maximizing the retail payoff function will give us the tradeoff curve between CS and RP with consumer-based decentralized storage. The following theorem characterizes the shape of the Pareto front of the CS-RP tradeoffs in the presence of decentralized storage integration.

**Theorem 4:** Let the social welfare and retail profit maximization prices with decentralized storage integration be \( \pi_{sw} \) and \( \pi_{sw} \), respectively.

1. The social welfare maximization price is \( \pi_{sw} = \lambda \). The resulting retail profit is \( \pi_{rb}(\lambda) = 0 \). The corresponding consumer surplus is greater than that in absence of storage, i.e., \( CS_{rb}(\lambda) \geq CS_{rb}(\lambda) \).

2. Assume that \( Q(\bar{\pi}) > 3Q(\lambda) \), where \( \bar{\pi} = \bar{\pi} \), which is the cut-off price resulting in zero demand. There exists a threshold \( \xi \) such that, when \( B \leq \xi \), the maximized profit is less than that in absence of storage integration, i.e., \( \pi_{rb}(\lambda) \leq \pi_{rb}(\lambda) \).

3. The Pareto front with decentralized integration is always inside that of the centralized integration with the same storage parameters.

**Proof:** When the preference weight factor on consumer surplus \( \eta = 1 \), the retailer’s payoff function is social welfare. Notice that

\[
SW_{rb}(\lambda) = \pi_{rb}(\lambda) + CS_{rb}(\lambda) = \pi(\lambda) + CS_{rb}(\lambda) + Q(\lambda)
\]

\[
\geq \pi(\lambda) + CS_{rb}(\lambda) - \lambda^T r(\pi) - \psi^T r(\pi) - \psi^T r^{-}(\pi)
\]

\[
= \pi(\lambda) + CS_{rb}(\lambda) + Q(\lambda) - \lambda^T r(\pi),
\]

for any \( \pi \), which means that the social welfare maximization price is \( \lambda \), resulting retail profit is 0, and the maximized social welfare is increased by \( Q(\lambda) \). Therefore, the social welfare maximization point is outside the original trade-off curve.

When the preference weight factor \( \eta = 0 \), the retailer’s payoff function is the retail profit. Without storage, the optimal
price is \( \pi^0 = (\hat{\lambda} + \hat{\pi})/2 \). With the decentralized consumer-based storage, the consumer surplus is increased by \( Q(\pi_{ds}^0) \), while the retail profit is changed by \(- (\pi_{ds}^0)^T r(\pi_{ds}^0) - \hat{\lambda}^T r(\pi_{ds}^0) \). Also, we denote \( \pi_{ds} = \pi^0 + \Delta \pi \). We know \( Q(\pi) \) is a piecewise linear function of \( \pi \). Therefore,

\[
Q(\pi_{ds}^0) = Q(\hat{\pi} + \hat{\lambda}/2 + \Delta \pi), \\
\geq Q(\hat{\pi})/2 - \max_x \{- (\Delta \pi)^T r(\pi)\}/2 \\
= Q(\hat{\lambda}) + (Q(\hat{\pi}) - 3Q(\hat{\lambda}))/2 \\
- \max_x \{- (\Delta \pi)^T r(\pi)\}, \tag{19}
\]

Since \( Q(\hat{\pi}) > 3Q(\hat{\lambda}) \), there exists a threshold \( \xi \) s.t. when the storage size is less than \( \xi \), \( \Delta \pi \) is small enough to make \( Q(\pi_{ds}^0) > Q(\hat{\lambda}) \). Therefore, the RP changes,

\[
(\pi_{ds}^0)^T r(\pi_{ds}^0) - \hat{\lambda}^T r(\pi_{ds}^0) \\
\leq -Q(\pi_{ds}^0) - \psi^x^T r^*(\pi_{ds}^0) - \psi^T r^*(\pi_{ds}^0) - \hat{\lambda}^T r(\pi_{ds}^0) \\
< -Q(\hat{\lambda}) - \psi^x^T r^*(\pi_{ds}^0) - \psi^T r^*(\pi_{ds}^0) - \hat{\lambda}^T r(\pi_{ds}^0) \leq 0.
\]

We have the maximized profit decreased with small storage.

For a particular \( \eta \in (0, 1) \), assume the optimal price with decentralized consumer-based storage is \( \pi_{ds}(\eta) \). We use this price for the case with centralized utility-based storage. The change of social welfare is non-negative. The corresponding point \( x \) has decreased consumer surplus and increased retail profit. Since the slope for that point is \(-\eta\), all the left points on the trade-off curve with decentralized storage have less social welfare, this point \( x \) is outside the trade-off curve with consumer-based storage. On the other hand, \( \pi_{ds}(\eta) \) is a feasible price for the case with centralized utility-based storage and the corresponding point is inside the trade-off curve with utility-based storage. Therefore, the centralized utility-based storage results in a trade-off curve completely outside the one with decentralized consumer-based storage.

Theorem 4 shows that, under some conditions, maximized retail profit with decentralized storage decreases while the maximized social welfare increases, comparing with the case without storage. Therefore, the new trade-off curve is inside the original curve on the left side and outside the original curve on the right side; the two curves will intersect with each other, similar to decentralized renewable integration.

Since demand level varies across different hours, the cut-off price \( \tilde{\pi} \) will lead to high arbitrage opportunity. Therefore, the condition \( Q(\tilde{\pi}) > 3Q(\hat{\lambda}) \) is reasonable in practice. For the setup in our following simulation, the arbitrage profit with cut-off price \( \tilde{\pi} \) is much higher than with wholesale price, \( Q(\tilde{\pi}) > Q(\hat{\lambda}) \), i.e., the condition of Theorem 4 is satisfied.

Numerical simulation results are plotted in Fig. 9. For the decentralized case, we assume 20% of the consumers have the storage devices. For the centralized model, we assume utility-based storage has the same size as the aggregated consumer-based storage to make fair comparison.

Fig. 8 shows that when the retailer has access to the storage devices, the Pareto front is shifted upward by \( Q(\hat{\lambda}) \) and the social welfare point becomes economically viable.

On the other hand, as for the consumer-based storage, when the weight on consumer surplus \( \eta = 1 \), the retail profit remains zero, and the consumer surplus increases by \( Q(\hat{\lambda}) \). When \( \eta = 0 \), the retailer maximizes its own profit. The leftmost point on the new Pareto front shows that the consumer surplus increases while the retail profit decreases at a much faster rate comparing with the original tradeoff curve. In this case, the profit maximization point is inside the original Pareto front.

The Pareto front with consumer-based storage crosses with the original Pareto front. This means that only when the retailer is operating on the right of the cross point, consumer-based storage can benefit the retail market. On the contrary, the Pareto front with utility-based storage is outside the original Pareto front. Therefore, utility-based storage always benefits the retail market.

Another conclusion from Theorem 4 is that utility-based storage results in an enlarged Pareto front comparing with the trade-off curve with consumer-based storage of the same size. This conclusion can be also identified from Fig. 8. Comparing the trade-off curves with utility-based storage and consumer-based storage, we can see that the former one is completely outside the latter, which means that having utility-based storage brings more benefit to the retail market than consumer-based one, if no other considerations are taken.

Furthermore, for utility-based storage, the optimal DAHP prices won’t change. While for consumer-based storage, we plotted the profit maximization prices with different storage implementation levels as shown in Fig. 9. Due to the arbitrage opportunity with consumer-based storage, the price becomes flatter. This shows that only consumer-based storage will change the consumers’ energy consumption pattern.
VI. CONCLUSION

In this paper, we investigate the problem of integrating renewable and storage in distribution systems. We compare the centralized integration by the utility and decentralized integration by consumers. By examining the change of the optimal CS-RP tradeoffs, we gain insights into how benefits of integrations are distributed and the effects of integration.

Our analysis suggests that there is potential benefits of centralized integration by coordinating distributed generation and storage operation. We should note that the centralized integration considered here means only that the objective of integration is global and resources are owned by the operator. The actual implementation of control and communication algorithms that facilitate the centralized integration can very well be implemented locally in a decentralized architecture.

In this paper, we considered a simplified case to draw a clear contrast on the two types of integration models. To this end, we have based our analysis on a Stackelberg game model that assumes complete and perfect information. In practice, more complicated consumer-utility interactions are likely to exist, especially when demand models are unknown. It is possible that decentralized integration may exhibit advantage over centralized integration. This is an interesting and certainly more complex situation to investigate separately.

REFERENCES

[1] P. Joskow, “Capacity payments in imperfect electricity markets: need and design,” Utility Policy, vol. 16, pp. 159–170, 2008.
[2] D. Cai, S. Adlakha, S. Low, P. DeMartini, and K. M. Chandy, “Impact of residential PV adoption on retail electricity rates,” Energy Policy, vol. 62, pp. 830–843, 2013.
[3] P. Bronski et al., “The economics of grid defection: when and where distributed solar generation plus storage competes with traditional utility service,” Rocky Mountain Institute, Tech. Rep., Feb. 2014.
[4] S. Borenstein, M. Jaske, and A. Rosenfeld, “Dynamic Pricing, Advanced Metering, and Demand Response in Electricity Markets,” Recent Work, Center for the Study of Energy Markets, UC Berkeley, 2002.
[5] S. Borenstein, “The long run efficiency of real-time electricity pricing,” The Energy Journal, vol. 26, no. 3, 2005.
[6] R. Sioshansi and W. Short, “Evaluating the impacts of real-time pricing on the usage of wind generation,” IEEE Transactions on Power Systems, vol. 24, no. 2, May 2009.
[7] M. Roozbehani, M. A. Dahleh, and S. K. Mitter, “Volatility of Power Grids Under Real-Time Pricing,” IEEE Transactions on Power Systems, 2012.
[8] N. Hopper, C. Goldman, and B. Neenan, “Demand Response from Day-Ahead Hourly Pricing for Large Customers,” Electricity Journal, 2006.
[9] P. Luh, Y. C. Ho, and R. Muradidharian, “Load Adaptive Pricing: An Emerging Tool for Electric Utilities,” IEEE Transactions on Automatic Control, vol. AC-27, no. 2, April 1982.
[10] L. Chen, N. Li, S. H. Low, and J. C. Doyle, “Two market models for demand response in power networks,” in IEEE International Conference on Smart Grid Communications, 2011.
[11] N. Li and S. H. L. Lijun Chen, “Optimal demand response based on utility maximization in power networks,” in PIEEE Power Engineering Society General Meeting, 2011.
[12] A. Papavassiliou and S. Oren, “Integrating renewable energy contracts and wholesale dynamic pricing to serve aggregate flexible loads,” in IEEE Power and Energy Society General Meeting, 2011.
[13] ——, “Coupling wind generators with deferrable loads,” in IEEE Energy2030, Nov. 2008, pp. 1–7.
[14] M. Carrion, A. Conejo, and J. Arroyo, “Forward Contracting and Selling Price Determination for a Retailer,” IEEE Transactions on Power System, vol. 32, no. 4, November 2007.
[15] A. Conejo, R. Garcia-Bertrand, M. Carrion, A. Caballero, and A. Andres, “Optimal Involvement in Futures Markets of a Power Producer,” IEEE Transactions on Power Systems, vol. 23, no. 2, May 2008.
[16] R. Sioshansi, P. Denholm, T. Jenkin, and J. Weiss, “Estimating the value of electricity storage in pjm: Arbitrage and somewellfare effects,” Energy Economics, 2009.
[17] R. Sioshansi, “Welfare impacts of electricity storage and the implications of ownership structure,” The Energy Journal, 2010.
[18] A. Faghih, M. Roozbehani, and M. Dahleh, “On the value and price responsiveness of ramp-constrained storage,” Energy Conversion and Management, 2013.
[19] Y. Xu and L. Tong, “On the Value of Storage at Consumer Locations,” in 2014 IEEE PES General Meeting, July 2014.
[20] J. Taylor, D. Callaway, and K. Pooila, “Competitive energy storage in the presence of renewables,” Power Systems, IEEE Transactions on, pp. 895–906, 2013.
[21] L. Jia and L. Tong, “Optimal pricing for residential demand response: A stochastic optimization approach,” in 2012 Allerton Conference on Communication, Control and Computing, Oct. 2012.
[22] ——, “Day ahead dynamic pricing for demand response in dynamic environments,” in 52nd IEEE Conference on Decision and Control, Dec. 2013.
[23] ——, “Renewable in distribution networks: centralized vs. decentralized integration,” in Proc. 2015 IEEE Power and Energy Society General Meeting (PESGM), Denver, Colorado, July 2015.
[24] D. Bargiotas and J. Birdwell, “Residential air conditioner dynamic model for direct load control,” IEEE Transactions on Power Delivery, vol. 3, no. 4, pp. 2119–2126, Oct. 1988.

Lang Tong (S’87,M’91,SM’01,F’05) is the Irwin and Joan Jacobs Professor in Engineering of Cornell University and the site director of Power Systems Engineering Research Center (PSERC). He received the B.E. degree from Tsinghua University in 1985, and M.S. and Ph.D. degrees in electrical engineering in 1987 and 1991, respectively, from the University of Notre Dame. He was a Postdoctoral Research Affiliate at the Information Systems Laboratory, Stanford University in 1991. He was the 2001 Cor Wit Visiting Professor at the Delft University of Technology and had held visiting positions at Stanford University and the University of California at Berkeley. Lang Tong’s research is in the general area of statistical inference, communications, and complex networks. His current research focuses on inference, optimization, and economic problems in energy and power systems. He received the 1993 Outstanding Young Author Award from the IEEE Circuits and Systems Society, the 2004 best paper award from IEEE Signal Processing Society, and the 2004 Leonard G. Abraham Prize Paper Award from the IEEE Communications Society. He is also a coauthor of seven student paper awards. He received Young Investigator Award from the Office of Naval Research. He was a Distinguished Lecturer of the IEEE Signal Processing Society.

Liyan Jia received his B.E. degree from Department of Automation, Tsinghua University in 2009. He is currently working toward the Ph.D. degree in the School of Electrical and Computer Engineering, Cornell University. His current research interests are in smart grid, electricity market and demand response.