Beamforming design with proactive interference cancelation in MISO interference channels

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Abstract

In this paper, we design coordinated beamforming at base stations (BSs) to facilitate interference cancelation at users in interference networks, where each BS is equipped with multiple antennas and each user is with a single antenna. By assuming that each user can select the best decoding strategy to mitigate the interference, either canceling the interference after decoding when it is strong or treating it as noise when it is weak, we optimize the beamforming vectors that maximize the sum rate for the networks under different interference scenarios and find the solutions of beamforming with closed-form expressions. The inherent design principles are then analyzed, and the performance gain over passive interference cancelation is demonstrated through simulations in heterogeneous cellular networks.

Keywords: Coordinated beamforming; Proactive interference cancelation; Interference channels; Heterogeneous networks

1 Introduction

One of the key features of the fifth generation cellular networks is ultra dense and heterogeneous [1], where the interference generated by different base stations (BSs) is more complicated. Depending on the locations, the users may experience different levels of interference.

Various BS cooperation techniques have been proposed to mitigate inter-cell interferences. A stronger form of cooperation is so called “CoMP-JP” (Coordinated Multi-Point Transmission with Joint Processing) [2, 3], where the antennas from multiple BSs act as a single antenna array, and the inter-cell interference is transferred into useful signals. However, this kind of schemes require sharing large amounts of user data over finite-capacity backhaul links and assume that BSs have full channel state information (CSI) of all the active users in the system. In contrast, the CoMP coordinated beamforming (CB) scheme only requires sharing the CSI of the interfered users among cooperated BSs and is therefore more feasible for practical implementations [4–10].

For multi-input-multi-output (MIMO) interference channels, the optimal beamforming design is not an easy task, because the achievable rate of each user depends on the beamforming of all BSs [11]. Most of the existing researches focus on linear transceiver design, where the signal and interference are separated into orthogonal subspaces. However, if each coordinated BS does not have more antennas than the number of users in the network, we must perform user scheduling first so that the orthogonal-based CB can remove all the interferences in the scheduled user group. On the other hand, if the interference is very weak or very strong, it is a waste of spatial resource to provide an orthogonal subspace for each interference. In fact, for weak interference channels, treating the interference as noise is optimal [12, 13]. For strong interference channels, interference cancelation can achieve the capacity [14]. For the more general mixed interference channels, the capacity region is unknown and the achievable sum-rate expression is non-convex over the precoding matrices, there is no efficient algorithm available to find the optimal precoding matrices [15].

In [16], six interference scenarios for a single-antenna two-cell network were characterized, where the users respectively experience very strong, strong, mixed 1, mixed 2, weak, and very weak interferences. For each scenario, a corresponding transmission scheme to achieve the capacity or the best known achievable rate was
designed, and the concept of proactive interference cancelation was proposed for strong and mixed interference scenarios. The basic idea of proactive interference cancelation is to guarantee strong interference to be decodable and hence can be thoroughly canceled at the receiver by designing the transmitter. This is distinct from an existing interference cancelation scheme, which waits for the opportunity until the interference becomes strong enough to be decodable [17]. In [18], the idea was extended to MIMO interference channels in the mixed interference scenario, where a coordinated precoding method was developed to facilitate proactive interference cancelation. Since the sum-rate expression is a non-convex function of the precoding matrices, an iterative solution was found through convex relaxation.

In this paper, we consider a transmission scheme design for multi-input-single-output (MISO) interference channels. In [19], a parameterization of the beamforming that achieves the Pareto boundary of the achievable rate region was proposed, where a brute-force searching is required to find the solutions. In [20], a more efficient method was proposed to find the Pareto-optimal beamforming vectors, which however needs a line searching, and to solve a cubic equation at each search point.

Considering that closed-form transceivers are highly desirable for practical systems, we employ an alternative approach to design the coordinated beamforming that assists proactive interference cancelation for MISO interference channels. Specifically, we assume that each receiver is able to choose the best decoding strategy to mitigate the interference, either decoding the interference first and then canceling it when it is strong or treating it as noise when it is weak. To maximize the sum rate, the strong interference might need to be further strengthened to increase the interference-to-signal-plus-noise ratio (ISNR), and the weak interference might need to be further weakened to increase the signal-to-interference-plus-noise ratio (SINR). Inspired by such an intuition, we formulate the optimization problem for designing linear beamforming that maximizes the sum rate with given decoding methods under different interference scenarios. Beamforming vectors with explicit expressions are then provided. Simulation results show that the proposed transmission scheme is superior to existing schemes in heterogeneous networks (HetNets).

The rest of this paper is organized as follows. In Section 2, we first introduce the system model and the transmission scheme with proactive interference cancelation. Then, we formulate the optimization problem to find the beamforming that maximizes the sum rate in Section 3. The closed-form solution of the corresponding problem in four scenarios is found in Section 4, and the performance in HetNets is evaluated in Section 5. Finally, Section 6 concludes the paper.

2 System model and transmission scheme
In this section, we introduce the system model and the transmission scheme with proactive interference cancelation.

2.1 System model
Consider a HetNet scenario as shown in Fig. 1, where one macro-cell coexists with pico-cells in the same frequency band. To obtain a closed-form solution and gain useful insight, we first consider a two-cell MISO network consisting of one macro-cell and one pico-cell in the optimization and then extend the designed beamforming to multi-cell networks.

For the convenience of expression, we assume the macro-BS and pico-BS as BS$_1$ and BS$_2$, respectively. Correspondingly, the macro-user is user 1 and the pico-user is user 2. Each BS knows the channel information from itself to both users. The $i$-th BS, $i \in \{1, 2\}$, is equipped with $M_i$ antennas, and each user is equipped with a single antenna.

The symbol received at user $i$ is

$$y_i = h_i^H v_i x_i + n_i, \quad i, j \in \{1, 2\}, \quad j \neq i$$

where $h_{ij} \in \mathbb{C}^{M_i \times M_j}$ denotes the channel vector from BS$_i$ to user $j$, $x_i$ is the symbol transmitted by BS$_i$ with power $\mathbb{E}[|x_i|^2] = P_i$, $v_i \in \mathbb{C}^{M_i}$ is the transmit beamforming vector at BS$_i$ with unit-norm $|v_i| = 1$, and $n_i$ is the Gaussian white noise at user $i$ with zero mean and unit variance.

2.2 Transmission scheme
The transmission scheme with proactive interference cancelation includes transmit beamforming and decoding.

![Fig. 1 The coexistence of one macro-cell and multiple pico-cells in heterogeneous networks](image-url)
We first decide the decoding methods for two users according to interference scenarios as follows. (a) When both users suffer weak interference, the desired signals are decoded directly by treating the interference as noise at both users. (b) When one user suffers strong interference while the other suffers weak interference, the strong interference is decoded and subtracted before the desired signal is decoded, and the weak interference is simply treated as noise. (c) When both users suffer strong interference, both users first decode and subtract the interference and then decode the desired signals.

A similar classification of the interference scenarios has been introduced in [15] and [21]. Since we do not know whether the interference is strong or weak before beamforming, we will find the optimal beamforming vectors for each of the three decoding methods and then choose the scheme that achieves the highest sum rate.

3 Problem formulation

Given the decoding method at each user, we can obtain the sum rate as a function of the beamforming vector, from which we can formulate the optimization problem to find the beamforming that maximizes the sum rate.

(a) Both users treat the interference as noise: When both users are subject to weak interference that is not able to be decoded correctly, the interference can be treated as noise at each user. If the SINR at each user is high, i.e., SINR$_i > 1$, where

\[
\text{SINR}_i = \frac{P_i |h_{ij}^H v_i|^2}{P_j |h_{ij}^H v_j|^2 + 1}, \quad i, j \in \{1, 2\}, \quad j \neq i, \tag{2}
\]

then the achievable sum rate can be approximated as

\[
R^\text{weak}(v_1, v_2) = 2 \sum_{i=1}^{2} \log_2 (1 + \text{SINR}_i) \approx 2 \sum_{i=1}^{2} \log_2 (\text{SINR}_i). \tag{3}
\]

This approximation will lead to at most 1 bps/Hz loss in an achievable rate of each user in this scenario, because

\[
\log_2 (1 + t) - \log_2 t = \log_2 (1 + t^{-1}) \leq 1 \quad (t \geq 1). \tag{4}
\]

(b) One user decodes the interference: This is a scenario of mixed interference. When user 1 suffers strong interference while user 2 experiences weak interference, the strong interference should be decoded and canceled at user 1 and the weak interference at user 2 can be treated as noise. Similar to the previous case, we assume high SINR at user 2, i.e., SINR$_2 > 1$. At user 1, the interference should be much stronger than the desired signal and the noise in order to be decodable, hence we can apply a high ISNR assumption, i.e., ISNR$_1 \gg 1$, where

\[
\text{ISNR}_1 = \frac{P_i |h_{ij}^H v_j|^2}{P_j |h_{ij}^H v_j|^2 + 1}, \quad i, j \in \{1, 2\}, \quad j \neq i. \tag{5}
\]

User 1 decodes and subtracts the interference caused by BS$_2$, and then the desired signal from BS$_1$ is decoded in an interference-free environment, thus the achievable rate of user 1 is \( \log_2 (1 + P_i |h_{11}^H v_1|^2) \). The achievable rate of user 2 is upper bounded by \( \log_2 (1 + \text{ISNR}_1) \) and \( \log_2 (1 + \text{SINR}_2) \) simultaneously, since the signal from BS$_2$ should be decodable both at user 1 and user 2. Similar to the previous case, under the assumption of high ISNR$_1$ and SINR$_2$, the achievable sum rate can be approximated as

\[
R^\text{mixed}_1(v_1, v_2) \approx \log_2 (1 + P_i |h_{11}^H v_1|^2) + \log_2 (\min(\text{ISNR}_1, \text{SINR}_2)). \tag{6}
\]

If user 1 treats the interference as noise and user 2 decodes it, the achievable sum rate can be approximated similarly to (6) as

\[
R^\text{mixed}_2(v_1, v_2) \approx \log_2 (1 + P_2 |h_{22}^H v_2|^2) + \log_2 (\min(\text{ISNR}_2, \text{SINR}_1)). \tag{7}
\]

(c) Both users decode the interference: When both users suffer strong interference, they decode and cancel the interference first and then decode their desired signals. Since the interference should be much stronger than the desired signal and the noise, it is reasonable to assume high ISNR at each user, i.e., ISNR$_i \gg 1$, \( i = 1, 2 \).

To ensure the interference caused by BS$_1$ to be decodable at user 2, the achievable rate of user 1 should be upper bounded by \( \log_2 (1 + \text{ISNR}_2) \). Similarly, the achievable rate of user 2 should be upper bounded by \( \log_2 (1 + \text{ISNR}_1) \). After decoding the interference, each user decodes the desired signal without interference. Therefore, the achievable rate of user \( i \) is also upper bounded by \( \log_2 (1 + P_i |h_{ii}^H v_i|^2) \). Then, the achievable sum rate can be approximated as

\[
R^\text{strong}(v_1, v_2) \approx \sum_{i=1, i \neq 1}^{2} \log_2 (\min (\text{ISNR}_i, 1 + P_i |h_{ii}^H v_i|^2)). \tag{8}
\]

The approximation in case (c) will lead to at most 1 bps/Hz per-user rate loss as in case (a), and in case (b), it will loss at most 1 bps/Hz at only one user.

Among these cases, the best achievable scheme will be selected as the final transmission scheme. Such problem to find the optimal beamforming can be formulated as

\[
\max_{v_1, v_2} \left( R^\text{weak}, R^\text{mixed}_1, R^\text{mixed}_2, R^\text{strong} \right). \tag{9a}
\]
s.t. \( \|v_i\| = 1, \ v_i \in \mathbb{C}^{M_2}, i = 1, 2. \)  \hspace{1cm} (9b)

4 Beamforming design with closed form

In this section, we strive to find a closed-form solution of problem (9). To this end, we need to find the beamforming vectors that respectively maximize the achievable sum rates in four scenarios, \( R^{\text{weak}}, R^{\text{mixed1}}, R^{\text{mixed2}}, \) and \( R^{\text{strong}}. \)

4.1 Both users treat the interference as noise

For the scenario where both users treat the interference as noise, the achievable sum rate \( R^{\text{weak}} \) in (3) is rewritten as

\[
\log_2 \left( \frac{P_1 |h_{11}^H v_1|^2}{P_1 |h_{12}^H v_1|^2 + 1} \cdot \frac{P_2 |h_{22}^H v_2|^2}{P_2 |h_{21}^H v_2|^2 + 1} \right).
\]

The maximization of (10) can be achieved by solving the generalized Rayleigh quotient problem as follows

\[
\max_{v_i} \frac{P_1 v_i^H h_i^H v_i}{v_i^H B_i v_i},
\]

whose solution is given by generalized eigenvalue decomposition

\[
h_i h_i^H v_i = \lambda_i B_i v_i,
\]

where \( B_i = P_i h_i h_i^H + I_{M_2} \) and \( \lambda_i \) is the unique nonzero eigenvalue of \( B_i^{-1} h_i h_i^H. \) Considering the unit-norm constraint of the beamforming vector, we can obtain

\[
v_i^{\text{weak}} = \frac{B_i^{-1} h_i}{\|B_i^{-1} h_i\|}, \quad i = 1, 2,
\]

which is one of the generalized eigenvectors associated to \( \lambda_i. \) Note that this result was also obtained in [7]. From the optimization problem, we can see that the beamforming vector is to maximize the signal-to-leakage-plus-noise ratio (SLNR).

4.2 One user decodes the interference

For the scenario where user 1 suffers strong interference and user 2 experiences weak interference (the scenario where user 1 experiences weak interference and user 2 suffers strong interference is similar and hence omitted), from (6), the achievable sum rate \( R^{\text{mixed}} \) can be expressed as

\[
\log_2 \left( \min \left( P_2 |h_{12}^H v_2|^2, P_2 |h_{22}^H v_2|^2 \frac{|h_{12}^H v_2|^2}{|h_{21}^H v_1|^2 + 1} \right) \right).
\]

Since \( v_1 \) appears only in the second term of the minimum function above, the optimal solutions of \( v_1 \) and \( v_2 \) that maximize (14) can be found successively. Specifically, we can first find \( v_1 \) by solving the generalized Rayleigh quotient problem as follows

\[
\max_{v_1} \frac{v_1^H B_1 v_1}{v_1^H B_2 v_1},
\]

whose solution is the generalized eigenvector associated to the largest generalized eigenvalue \( \lambda_{\text{max}}, \) which is

\[
B_1 v_1 = \lambda_{\text{max}} B_2 v_1.
\]

Thus, we can obtain

\[
v_1^{\text{mixed}} = v_{\text{max}} \left( B_2^{-1} B_1 \right),
\]

where \( v_{\text{max}}(A) \) is the unit-norm eigenvector corresponding to the largest eigenvalue of \( A. \) Then, we find the solution of \( v_2. \) Substituting \( \lambda_{\text{max}} \) into (14), we can obtain the optimization problem for \( v_2 \) as follows

\[
\max_{v_2} \min \left( P_2 |h_{12}^H v_2|^2, P_2 |h_{22}^H v_2|^2 \lambda_{\text{max}} \right).
\]

Since \( \lambda_{\text{max}} \) is a positive real number, (18) can be further simplified as

\[
\max_{v_2} \min \left( |h_{12}^H v_2|, |\sqrt{\lambda_{\text{max}}} h_{22}^H v_2| \right).
\]

To better understand problem (19), we provide its geometric explanation in Fig. 2. Since \( v_2 \) is a unit-norm vector in \( \mathbb{C}^{M_2}, \) finding the solution of problem (19) is equivalent to finding a direction vector that maximizes the minimum of projections of \( h_{12} \) and \( \sqrt{\lambda_{\text{max}}} h_{22} \) on it.

**Case 1:** If the projection of \( \sqrt{\lambda_{\text{max}}} h_{22} \) on the direction vector \( \frac{h_{12}}{|h_{12}|} \) is bigger than \( \|h_{12}\|, i.e., \sqrt{\lambda_{\text{max}}} |h_{12} h_{22}| \geq |h_{12}|^2 \) as shown in Fig. 2a, (19) is upper bounded by \( |h_{12}^H v_2|, \) which is the maximum of \( |h_{12}^H v_2|. \) Then the optimal solution is

\[
v_2^{\text{mixed}}(1) = \frac{h_{12}}{|h_{12}|}.
\]

**Case 2:** If the projection of \( h_{12} \) on the direction vector \( \frac{\sqrt{\lambda_{\text{max}}} h_{22}}{|\sqrt{\lambda_{\text{max}}} h_{22}|} \) exceeds \( \|\sqrt{\lambda_{\text{max}}} h_{22}\|, i.e., \|h_{12}^H h_{22}\| \geq \sqrt{\lambda_{\text{max}}} |h_{22}|^2 \) as shown in Fig. 2b, the function in (19) is upper bounded by \( \sqrt{\lambda_{\text{max}}} |h_{22}|^2, \) which is the maximum of \( |\sqrt{\lambda_{\text{max}}} h_{22}^H v_2|. \) The optimal solution is

\[
v_2^{\text{mixed}}(2) = \frac{h_{22}}{|h_{22}|}.
\]

**Case 3:** Besides these two cases, the optimal solution will be obtained when the following equality holds

\[
|h_{12}^H v_2| = |\sqrt{\lambda_{\text{max}}} h_{22}^H v_2|,
\]

which is due to the nature of the maximization of the minimum function and the continuity of the two terms. The solution will be located in a two-dimensional subspace of \( \mathbb{C}^{M_2} \) spanned by \( h_{12} \) and \( h_{22}. \)
To find the solution of $v_2$ from (22), we need to consider two subcases based on the projection angle of $h_{12}$ and $h_{22}$, as shown in Fig. 3.

**Case 3(a):** If the real part of $h_{12}^H h_{22}$ is positive, i.e., $\Re (h_{12}^H h_{22}) > 0$, the solution of $v_2$ is in the direction of the altitude of the acute triangle as shown in Fig. 3(a). Denote $a = h_{12} - \sqrt{\lambda_{\max}} h_{22}$, which is the third edge of the triangle. Let $h_{12} + \alpha h_{22}$ denote an arbitrary vector in the two-dimensional subspace, where $\alpha$ is the weighting coefficient. Since $v_2^{\text{mixed}}$ is perpendicular to $a$, by solving the equation $a^H (h_{12} + \alpha h_{22}) = 0$, we obtain the optimal weighting coefficient as $\alpha^* = -\frac{a^H h_{12}}{a^H h_{22}}$. Then, the solution is

$$v_2^{\text{mixed}}(3) = \frac{h_{12} + \alpha^* h_{22}}{\|h_{12} + \alpha^* h_{22}\|}.$$  

**Case 3(b):** If $\Re (h_{12}^H h_{22}) \leq 0$, the solution of $v_2$ is in the direction of the altitude of the complementary triangle, as shown in Fig. 3(b). Denote $b = h_{12} + \sqrt{\lambda_{\max}} h_{22}$, which is the third edge of the complementary triangle. Similar to Case 3(a), since $v_2^{\text{mixed}}$ is perpendicular to $b$, by solving $b^H (h_{12} + \beta h_{22}) = 0$, we obtain the optimal weighting coefficient as $\beta^* = -\frac{b^H h_{12}}{b^H h_{22}}$ and obtain the solution in this subcase as

$$v_2^{\text{mixed}}(4) = \frac{h_{12} + \beta^* h_{22}}{\|h_{12} + \beta^* h_{22}\|}.$$  

### 4.3 Both users decode the interference

In a strong interference scenario, we maximize the achievable sum rate $R_{\text{strong}}$ in (8), which can be written as

$$\log_2 \left( \prod_{i=1}^{2} \min \left( \frac{P_i |h_{ii}^H v_i|^2}{P_j |h_{ij}^H v_j|^2 + 1 + P_i |h_{ii}^H v_i|^2}, 1 + P_i |h_{ii}^H v_i|^2 \right) \right).$$  

(25)
Denote $f_1(v_1) \triangleq P_1|h_{i1}^H v_1|^2 f_2(v_2) \triangleq P_2|h_{i2}^H v_2|^2$, and $g(v_1, v_2) \triangleq (1 + P_1|h_{i1}^H v_1|^2)(1 + P_2|h_{i2}^H v_2|^2)$. By expanding the product in (25), the maximization of (25) can be simplified as

$$\max_{v_1, v_2} \min\left(g(v_1, v_2), f_1(v_1), f_2(v_2), \frac{f_1(v_1)f_2(v_2)}{g(v_1, v_2)}\right),$$

(26)

whose solution is the maximum of the solutions to the following three subproblems.

$$\max_{v_1, v_2} g(v_1, v_2),$$

(27a)

$$\text{s.t.} \quad g(v_1, v_2) \leq \min\left(f_1(v_1), f_2(v_2)\right).$$

(27b)

$$\max_{v_1, v_2} f_1(v_1)f_2(v_2) \quad \frac{g(v_1, v_2)}{g(v_1, v_2)},$$

(28a)

$$\text{s.t.} \quad g(v_1, v_2) \geq \max\left(f_1(v_1), f_2(v_2)\right).$$

(28b)

$$\max_{v_1, v_2} \min\left(f_1(v_1), f_2(v_2)\right),$$

(29a)

$$\text{s.t.} \quad \min\left(f_1(v_1), f_2(v_2)\right) \leq g(v_1, v_2) \leq \max\left(f_1(v_1), f_2(v_2)\right).$$

(29b)

It is hard to solve these three optimization subproblems directly since the constraints are non-convex. To obtain beamforming vectors with explicit expressions, we find the solutions in the following way and allow a suboptimal solution.

**Case 1:** We first maximize (27a) without any constraints, and the solution is given by

$$v_i^{\text{strong}}(1) = \frac{h_{ii}}{\|h_{ii}\|}, \quad i = 1, 2.$$  

(30)

Then we substitute (30) into (27b) to check whether the constraint is satisfied.

If (27b) can be satisfied, $v_i^{\text{strong}}(1)$ in (30) is the optimal solution of problem (27). Moreover, it must be the global optimal solution of problem (26), since the maximization values of the objective functions of problems (28) and (29) must be smaller than the objective function in (27a), which is determined by (28b) and (29b).

If (27b) cannot be satisfied, the optimal solution of problem (27) is obtained when the equality in (27b) holds, which can be found from problem (29).

**Case 2:** Next, we maximize (28a) without any constraints, which is a generalized Rayleigh quotient problem. Similar to (13), we can obtain

$$v_i^{\text{strong}}(2) = \frac{B_i^{-1}h_i}{\|B_i^{-1}h_i\|}, \quad i = 1, 2.$$  

(31)

Substitute (31) into (28b) to check whether the constraint is satisfied. If (28b) can be satisfied, $v_i^{\text{strong}}(2)$ in (31) is the optimal solution of problem (28), which must be the global optimal solution of problem (26) as well. If (28b) cannot be satisfied, the optimal solution of problem (28) is obtained when the equality in (28b) holds. The problem can be included into problem (29) as well.

**Case 3:** Besides these two cases, the solution of problem (26) is obtained by solving the subproblem (29). If we remove the constraint in (29b), a simple solution can be obtained as

$$v_i^{\text{strong}}(3) = \frac{h_{ii}}{\|h_{ii}\|}, \quad i = 1, 2.$$  

(32)

This solution is optimal when it satisfies constraint (29b), otherwise it is suboptimal.

### 4.4 Summary and interpretation

The beamforming vectors optimized for the typical interference scenarios are summarized in Table 1, where in each scenario, the users apply different decoding methods. From the previous optimization procedure and the expression of each optimal beamforming vector, we can interpret the principle behind the optimal beamforming design for each scenario.

In weak interference scenario, the beamforming vectors at both BSs essentially maximize the SLNR, as we have explained in Section 4.1.

| Scenarios       | Sum rates | Beamforming vectors | Design principles |
|-----------------|-----------|---------------------|------------------|
| Weak interference | $g_{\text{weak}}$ | $v_1^{\text{weak}} = \frac{B_i^{-1}h_i}{\|B_i^{-1}h_i\|}$ | max $\text{SNR}_i$ |
| Mixed interference | $g_{\text{mixed}}$ | $v_1^{\text{mixed}} = \text{max}(B_1^{-1}B_1)$ | max $\text{SNR}_2$ |
| Strong interference | $g_{\text{strong}}$ | $v_1^{\text{strong}}(1) = \frac{h_{11}}{\|h_{11}\|}$ | max $\text{INR}_i$ |
In the mixed interference scenario where user 1 is subject to strong interference, the beamforming vector at BS$_1$ also maximizes the SLNR since BS$_1$ generates weak interference; while the beamforming vector at BS$_2$ depends on how strong the interference BS$_2$ might generate. Specifically, when the interference caused by BS$_2$ is not very strong, the beamforming vector is to match the cross-link channel $\mathbf{h}_{12}$ in order to maximize the INR$_1$, i.e., to strengthen the interference. When the interference from BS$_2$ is very strong, the beamforming vector only needs to match the direct-link channel $\mathbf{h}_{22}$ such that maximizes the SNR$_2$. When the interference level is in between, we need to find a trade-off between maximizing INR$_1$ and maximizing SNR$_2$.

In the strong interference scenario, the beamforming vector at each BS depends on the interference level. When the interference is very strong, the beamforming only maximizes the SNR. When the interference is not very strong, the beamforming should maximize the INR. When the interference level is in between, the beamforming is to maximize the leakage-to-signal-plus-noise ratio.

Compared with the conventional passive interference cancelation scheme, the proposed beamforming scheme requires higher complexity in implementations. The increased complexity mainly exists in two aspects. The first is the CSI exchange among the coordinated BSs, but this is a common requirement for all CB schemes. The second is the BS calculation before the beamforming selection. For the proposed scheme, each BS has to calculate the sum rate of several possible transmission schemes according to different decoding sequence, and for each decoding sequence, there is a corresponding beamforming design. Finally, each BS will choose the beamforming vector that results in the highest sum rate. However, since the involved calculations are all in closed form, the increased complexity is not high.

### 4.5 Extension to multiple pico-cells scenario

In a practical scenario where one macro-cell coexists with $N$ pico-cells, we can first select a pico-BS closest to the macro-user as BS$_2$, then design beamforming vectors $\mathbf{v}_1$ and $\mathbf{v}_2$ for the macro-BS and the selected pico-BS using the above principles as if there are only two cells and obtain their data rate $R_1$ and $R_2$.

For any other pico-BSs, assuming they are BS$_{v_i}$, $j = 3, 4, \ldots, N + 1$, beamforming vector $\mathbf{v}_j$ is designed according to the particular interference scenario considering the already determined $\mathbf{v}_1$ and $R_1$. For example, if pico-user $j$ is subject to weak interference from the macro-BS, the beamforming vector of BS$_j$ can be designed as in the weak interference scenario, i.e., maximizing the SLNR. Thus, we can obtain

$$
\mathbf{v}_j^{\text{weak}} = \frac{\mathbf{B}_j^{-1} \mathbf{h}_j}{\|\mathbf{B}_j^{-1} \mathbf{h}_j\|}, \quad j = 3, 4, \ldots, N + 1.
$$

If pico-user $j$ suffers strong interference from the macro-BS, beamforming vector $\mathbf{v}_j$ should guarantee the interference from the macro-BS to be decodable at pico-user $j$, i.e., BS$_j$ might proactively mismatch its direct-link channel to keep the required ISNR. Specifically, in order to ensure the interference from the macro-BS to be decodable, the ISNR at pico-user $j$ should be strong enough so that

$$
\log_2 (1 + \text{ISNR}_j) \approx \log_2 (\text{INR}_j) - \log_2 (1 + \text{SNR}_j) \geq R_1.
$$

Using the above constraint, after decoding and canceling the interference, the data rate of pico-user $j$ is upper bounded by

$$
R_j^{\text{strong}} = \log_2 (1 + \text{SNR}_j) \leq \log_2 (\text{INR}_j) - R_1.
$$

In addition, $R_j^{\text{strong}}$ is also upper bounded by the maximum of $\log_2 (1 + \text{SNR}_j)$, which is tight when $\mathbf{v}_j = \frac{\mathbf{h}_j}{\|\mathbf{h}_j\|}$. Denote the maximum of $\log_2 (1 + \text{SNR}_j)$ as $R_j^{\text{max}}$. The data rate of pico-user $j$ is

$$
R_j^{\text{strong}} = \min \left( \log_2 (\text{INR}_j) - R_1, R_j^{\text{max}} \right).
$$

Consequently, if $\log_2 (\text{INR}_j) - R_1 \geq R_j^{\text{max}}$, the optimal beamforming vector is

$$
\mathbf{v}_j^{\text{strong}}(1) = \frac{\mathbf{h}_j}{\|\mathbf{h}_j\|}, \quad j = 3, 4, \ldots, N + 1.
$$

Otherwise, the optimal beamforming vector is obtained when the equality in (35) holds, which is

$$
\log_2 (1 + P_j \|\mathbf{v}_j\|^2) = \log_2 (\text{INR}_j) - R_1.
$$

Denote $\theta_j$ as the projection angle between $\mathbf{h}_j$ and $\mathbf{v}_j$. The optimal beamforming vector $\mathbf{v}_j^{\text{strong}}(2)$ is an arbitrary unit-norm vector satisfying

$$
\cos \theta_j = \frac{1}{\|\mathbf{h}_j\|} \sqrt{\frac{\text{INR}_j - 2R_1}{P_j \cdot 2R_1}}, \quad j = 3, 4, \ldots, N + 1.
$$

### 5 Simulation results

In this section, we evaluate the performance of the proposed beamformers with proactive interference cancelation (PIC) in HetNets by comparing with other schemes.

To show the performance of the scheme that treats the interference as noise, we simulate the achievable rate of maximal-SLNR scheme [7], which is optimal for a weak interference scenario. To compare with spatially orthogonal transmission, the performance of zero-forcing-based CB (ZF-CB) [5] is shown. To demonstrate the performance gain of PIC over passive interference cancelation, we simulate a scheme that employs matched filter at each
and interference cancelation at each user (MF-IC) [17]. In addition, the Pareto-optimal beamforming method [20] is simulated and compared.

In the simulation, all BSs are equipped with two antennas, and each BS serves one user. The radiuses of the macro-cell and each pico-cell are 500 and 60 m, respectively. The transmit powers of the macro-BS and each pico-BS are 46 and 30 dBm, respectively. The noise power is determined by the cell edge SNR of the macro-cell, which is set as 5 dB. The path loss follows 3GPP channel model [22], and the small-scale channel is subject to Rayleigh fading. All the simulation results are obtained from 1000 channel realizations.

To show the performance under different interference scenarios, we first consider a two-cell HetNet and fix the position of the macro-user at 250 m away from the macro-BS and move the pico-BS from the macro-cell center to the macro-cell edge while keeping the relative position between the pico-BS and the pico-user fixed. The average sum rates of the considered transmission schemes are shown in Fig. 4. Comparing the sum rates achieved in different interference scenarios, we can see that as the pico-BS moves, the system successively experiences mixed 2, strong, mixed 1, and weak interference scenarios. Since both the beamforming designs and the decoding methods are different under different interference scenarios, the trend of the average sum rate of PIC varies in Fig. 4. In all scenarios, PIC approaches very closely to the Pareto-optimal scheme and outperforms all other schemes. The maximal-SLNR scheme is inferior to PIC in all scenarios except for the weak interference scenario. The average sum rate of ZF-CB is nearly constant in all interference scenarios, because the interference is orthogonal in spatial subspace to the desired signal. MF-IC has a similar trend with PIC but is inferior to PIC due to passively waiting for proper opportunities of canceling the interference.

Next, we will demonstrate the performance of PIC in HetNet with multiple pico-cells. As shown in Fig. 5, we consider a scenario where multiple pico-cells are randomly deployed in the macro-cell and the minimum
distance among the pico-BSs is 120 m. In the simulation, the position of the macro-user is still fixed at 250 m away from the macro-BS and the positions of pico-users are randomly distributed in the pico-cells. Figures 6 and 7 show the average sum rates and per-user rates of different schemes with the changing number of pico-cells, respectively. We can see that, although the sum rates of all five schemes increase as more pico-cells coexist, the PIC scheme increases the fastest. It is surprising that the Pareto-optimal scheme performs worse than the PIC scheme when the pico-cell number exceeds 5. As we have discussed, the Pareto-optimal scheme is originally designed for a two-cell scenario. To apply it in HetNet with multiple pico-cells, we use the same extension approach as used for a PIC scheme. We first select a pico-BS closest to the macro-user and design beamforming
vectors for the macro-BS and the selected pico-BS using the Pareto-optimal method as if there are only two cells. Then the beamforming vectors of other pico-BSs are designed according to the particular interference scenario considering the already determined $v_1$ and $R_1$. Since the Pareto-optimal scheme is not optimized for a multi-cell scenario, if the data rate of the macro-user is higher, it is possible to sacrifice the data rate of other pico-users and thus achieves a lower sum rate.

Figure 8 shows the cell edge per-user rates of the five schemes with the changing number of pico-cells. Note that the cell edge per-user rate is a statistic average counted from the worst served 5 % users, which does not imply the users are really located in the cell edge. It is shown that the PIC scheme outperforms the Pareto-optimal scheme and is much better than the maximal-SLNR, ZF-CB, and MF-IC schemes. For example, when 20 pico-cells coexist with the macro-cell, the cell edge per-user rate of the PIC scheme is about six times larger than that of the MF-IC scheme. As a consequence, the PIC scheme has great potential to improve the ubiquitous user experience in cellular networks.

6 Conclusions

In this paper, we proposed a transmission scheme for MISO interference channels. Specifically, we optimized the transmit beamforming that maximizes the achievable sum rate, given the best decoding methods for weak, mixed, and strong interference scenarios. Closed-form solutions of the optimal beamforming were obtained and the underlying design principles were interpreted. By proactively strengthening the interference with the optimized beamforming to ensure the interference to be correctly decoded and then subtracted at the receiver, the proposed scheme outperforms existing schemes of passive interference cancelation and zero-forcing beamforming, as demonstrated by simulation results.

Competing interests
The authors declare that they have no competing interests.

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