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Ce³⁺/Ce⁴⁺-Doped ZrO₂/CuO Nanocomposite for Enhanced Photocatalytic Degradation of Methylene Blue under Visible Light

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Abstract: In recent years, photocatalysis has been used as an environmentally friendly method for the degradation of organic pigments in water. In this study, Ce³⁺/Ce⁴⁺-doped ZrO₂/CuO as a mixed semiconductor oxide was successfully prepared by a one-step hydrothermal method. The Ce³⁺/Ce⁴⁺-doped ZrO₂/CuO has shown high degradation efficiency of methylene blue (MB), and the maximum degradation percentage was observed to be 94.5% at 180 min under irradiation visible light. The photocatalytic activity increases significantly by doping Ce³⁺/Ce⁴⁺ in ZrO₂/CuO for MB degradation. Ce³⁺/Ce⁴⁺ doping is shown to reduce the (e⁻/h⁺) recombination rate and improve the charge transfer, leading to enhanced photocatalytic activity of materials. The materials were characterized by X-ray diffraction (XRD), scanning electron microscopy (SEM), transmission electron microscopy (TEM), FTIR, EDS, BET and diffuse reflectance spectroscopy (DRS).

Keywords: Ce³⁺/Ce⁴⁺; mixed semiconductor oxide; hydrothermal; photocatalysis; methylene blue

1. Introduction

Water pollution is a global environmental problem as it can lead to the decomposition of aquatic ecosystems and affect human health. Contaminants can include organic or inorganic compounds, metal ions, dyes, phenols, pesticides and detergents. In which the pollution of natural and synthetic organic dyes poses challenges because of their high carcinogenic nature due to the fact they contain azo functional groups that, during decomposition, can form amines and benzidine [1]. Organic dyes are persistent organic pollutants that are resistant to decomposition through chemical and biological processes. The dye molecules are practically non-biodegradable, so they persist longer in the environment, creating potential hazards [2].

Today, water pollution is treated by applying technologies such as adsorption, coagulation, filtration and photocatalysis. In which the heterogeneous photocatalysis method has gained wide scientific attention with high potential for applications [3]. Zirconia (ZrO₂)-based photocatalysis for wastewater treatment is of great interest because ZrO₂ is a semiconductor oxide with high mechanical strength, is non-toxic, and has high chemical stability and biocompatibility. However, ZrO₂ has a large band gap; the E_g of ZrO₂ ranges from 3.25 to 5.1 eV, depending on the fabrication method [4]. Therefore, ZrO₂ needs to be irradiated with UV radiation to have a photocatalytic activity. UV radiation constitutes...
about 5% of the total electromagnetic radiation output from sunlight, limiting the practical applications of ZrO$_2$.

To improve the photocatalytic performance of ZrO$_2$, coupling with other semiconductor oxides has been shown to be an effective approach. The coupling produces mixed oxide semiconductors (MOS) that are capable of efficient charge separation due to the transition of electrons and holes generated from one semiconductor to another. CuO is often the semiconductor oxide of choice because it is a p-type semiconductor, has a small band gap of about 1.2 eV, is cheap and is environmentally friendly [5]. Renuka, L., et al., reported the synthesis of ZrO$_2$/CuO materials with excellent photocatalytic activity under visible light by a simple combustion method. The photocatalytic activity of ZrO$_2$/CuO obtained was 1.5 times higher than that of commercial P25 [6]. Nanda, B., et al., synthesized mesoporous CuO/ZrO$_2$–MCM–41 nanocomposites with high photocatalytic activity; the photo-reduction of Cr(VI) to Cr(III) had a 99% degradation efficiency in 30 min [7]. The synergistic effect between ZrO$_2$, CuO and TiO$_2$ oxides was also studied by Guerrero-Araque and Diana, et al. Co-catalysts are widely used to promote photocatalytic hydrogen production, especially CuO, which has shown a significant improvement in reaction rates [8].

Another use of low-photocatalytic activity is the electron-hole recombination process that occurs in the semiconductor oxide. In photocatalysis, the photocatalytic activity depends on the ability of the catalyst to create electron-hole pairs. Such an electron-hole pair is called an exciton. The excited electron and hole can recombine and release heat. Such exciton recombination leads to a decrease in photocatalytic activity. To reduce the recombination of electrons and holes, it is common to dope transition metal elements, especially rare earth, to prolongation of the exciton lifetime [9].

Recently, Piña-Pérez and Yanet, et al., doped Ce$^{3+}$/Ce$^{4+}$ into Al$_2$O$_3$, showing significantly improved electron-hole pair separation efficiency. This catalyst was chosen for the photodegradation of other phenolic derivatives such as 4–chlorophenol, p–cresol and 4–nitrophenol. Ce$^{3+}$/Ce$^{4+}$-doped Al$_2$O$_3$ synthesized by the sol-gel method showed better photocatalytic activity (TiO$_2$, P25 Degussa) [10]. The redox pair of Ce$^{4+}$/Ce$^{3+}$-doped α–β phase of Bi$_2$O$_3$ was reported by Akshatha, S., et al. The Ce$^{4+}$/Ce$^{3+}$-doped Bi$_2$O$_3$ created a synergistic effect to enhance the photocatalytic activity to degrade Alizarin red S dye [11].

To the best of our knowledge, there are many studies on the doping of Ce$^{3+}$/Ce$^{4+}$ ions into oxide semiconductors for photocatalysis. However, the doping of Ce$^{3+}$/Ce$^{4+}$ ions into mixed semiconductor oxide is a topic that has not been fully investigated. In this paper, we use the hydrothermal method to prepare Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO. The Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO mixed oxide semiconductor was used for the photocatalytic degradation of methylene blue (MB). X-ray diffraction (XRD), field emission scanning electron microscopy (FE-SEM), transmission electron microscopy (TEM), infrared spectroscopy (FT-IR), energy dispersive X-ray spectroscopy, spectrophotometry UV-Vis and Brunauer–Emmett–Teller (BET) were studied.

2. Materials and Methods

2.1. Preparation of the Ce$^{3+}$/Ce$^{4+}$-Doped ZrO$_2$/CuO Nanocomposites

The Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO nanocomposites were synthesized by the hydrothermal method. All chemicals were purchased from Merck (purity > 99%) and were used without further treatment: ZrCl$_4$, Cu(NO$_3$)$_2$.6H$_2$O, Ce(SO$_4$)$_2$.4H$_2$O, NaOH, C$_2$H$_5$OH, Methylene blue.

In a typical experiment, the molar ratio of ZrO$_2$/CuO was taken as 1:1, 10 mmol of ZrCl$_4$ and 10 mmol of Cu(NO$_3$)$_2$ were dissolved in 50 mL of deionized water, stirred in a magnetic stirrer at room temperature for 30 min. Next, 0–0.8 mmol Ce(SO$_4$)$_2$.6H$_2$O was added to the above solution. The mixture is stirred vigorously to obtain a clear and homogeneous mixture. After stirring these mixtures for 30 min, they were added to 10 mL of 2 M NH$_3$ aqueous solution to gel.

The gel was then transferred into a Teflon-lined 100 mL stainless steel autoclave, which was heated in an oven at 200 °C for 12 h (heated with a Nabatherm furnace, heating rate
5 °C/min). For natural cooling, the entire solution was centrifuged to collect the precipitate and washed with deionized water, and then dried at 80 °C. Pure ZrO$_2$ and CuO were prepared with the same procedure. Finally, all the prepared powders were calcined at 600 °C for 2 h and then allowed to cool to room temperature for further experiments.

2.2. Characterization

The morphology of the Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO nanocomposites was evaluated by using a field emission scanning electronic microscope (JEOL, JSM–7600F, JEOL Techniques, Tokyo, Japan). The surface morphology and microstructure of the nanocomposites were characterized by transmission electron microscopy (TEM) made with a (JEOL, JEM 1010, JEOL Techniques, Tokyo, Japan) operating at 200 kV. For the TEM analyses, the powders were dispersed in ethanol by sonication for 5 min.

FT-IR was performed in the range of 4000–400 cm$^{-1}$ with the help of (FT-IR using a Perkin–Elmer Spectrum BX spectrometer (PerkinElmer Inc., Wellesley, MA, USA) using KBr pellets to identify the functional groups present in the sample. EDS (Hitachi TM4000Plus Tabletop Microscope (Hitachi High-Tech Corporation, Tokyo, Japan)) was the determining element in the composites. The UV-Vis absorption spectrum was recorded using a (UV–1700 PharmaSpec, Shimadzu, Kyoto, Japan) UV-Visible spectrophotometer. The X-ray powder diffraction patterns were characterized using (XRD, D8 Advance, Bruker, Germany) a diffractometer at room temperature (Cu-K$\alpha$ radiation) with a nickel filter at a scan rate of 2°/min.

2.3. Dye Photodegradation

The photocatalytic activity of Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO nanocomposites was evaluated by investigating the degradation of methylene blue (MB). Using 30 mL of the MB solution with a dye concentration of 10 mgL$^{-1}$, which was illuminated under a light-emitting 300W Xenon lamp (sunlight simulation) at irradiance (1 Wcm$^{-2}$). Light filters were used to remove wavelengths $\lambda < 420$ nm. The distance from the lamp to the MB solution was 10 cm. To limit the influence of external light, the entire experimental system was placed in a dark chamber. The nanocomposite powder loaded into the MB solution was 20 mg. Then the suspension was stirred for 60 min in the dark to obtain balance adsorption and desorption equilibration of the system. About 3 mL was taken from the suspension at different irradiation times, it was then centrifuged at 4000 rpm for 10 min, and degradation measurements were performed by a UV-Vis spectrophotometer. The photodegradation efficiency was calculated using Equation (1):

$$\%H = \frac{C_0 - C_t}{C_0}.100$$  \hspace{1cm} (1)

where %H is the photodegradation efficiency, $C_0$ and $C_t$ are the concentrations of MB at time 0 and t (min), respectively.

3. Results

3.1. X-ray Diffraction

The XRD pattern of the Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO nanocomposites is shown in Figure 1. All the peaks in the XRD pattern are well indexed and have all crystallized as multiphase at Ce$^{3+}$/Ce$^{4+}$ different doping concentrations. ZrO$_2$/CuO and Ce$^{3+}$/Ce$^{4+}$ doped ZrO$_2$/CuO exists in three phases, namely tetragonal ZrO$_2$, monoclinic CuO and orthorhombic CuZrO$_3$. 
The diffraction peaks originating at $2\theta = \sim 30.48^\circ$, $34.35^\circ$, $50.30^\circ$, $50.65^\circ$ and $60.09^\circ$ correspond to (101), (200), (112), (220) and (202) planes of the tetragonal phase of ZrO$_2$ (JCPDS No. 00–050–1089), respectively. The diffraction peaks observed at $2\theta = \sim 35.68^\circ$, $38.89^\circ$, $48.93^\circ$, $53.62^\circ$, $61.70^\circ$, $65.97^\circ$ and $68.20^\circ$ are associated with (002), (111), (−202), (020), (−113), (022) and (113) planes, signifying the monoclinic phase of CuO (JCPDS No. 48–1548).

We also observed diffraction peaks at $2\theta = \sim 24.33^\circ$, $28.29^\circ$, $34.34^\circ$, $55.56^\circ$ and $61.72^\circ$ corresponded to (012), (112), (013), (313) and (402) planes of CuZrO$_3$ (PDF Card No. 00–043–0953), respectively. CuZrO$_3$ can be formed in a hydrothermal process, where the reaction between ZrO$_2$ and CuO occurs according to the chemical equation:

$$\text{ZrO}_2 + \text{CuO} \rightarrow \text{CuZrO}_3$$

It is interesting that when the Ce$^{3+}$/Ce$^{4+}$ doping concentration changes, the ratio between the phases changes. In the absence of Ce$^{3+}$/Ce$^{4+}$ doping, the material exists in all three phases, including tetragonal ZrO$_2$, monoclinic CuO and orthorhombic CuZrO$_3$. However, when increasing the doping concentration of Ce$^{3+}$/Ce$^{4+}$, the diffraction intensity of the CuZrO$_3$ phase decreased. According to the authors Dean, James, et al., reported that CuZrO$_3$ has a perovskite structure; this structure is less stable due to its low energy, which has a thermodynamic preference to decompose into CuO and ZrO$_2$ [12]. We believe that increasing the concentration of Ce$^{3+}$/Ce$^{4+}$ doping increases the ability of phase segregation to CuO and ZrO$_2$ is preferred.

### 3.2. Microstructure and Morphology of ZrO$_2$/CuO-Doped Ce$^{3+}$/Ce$^{4+}$ Nanocomposites

The microstructure of the Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO catalysts synthesized by the hydrothermal method was analyzed by FE-SEM. Figure 2a–d show that the Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO catalysts are spheres with non-uniform size distribution. When the Ce$^{3+}$/Ce$^{4+}$ doping concentration changed from 2 mol% to 8 mol%, the morphology of the catalysts was not significantly affected.

The size of the catalyst, as well as the surface area, greatly influence the photocatalytic efficiency. The small size of the material shows that the ability to adsorb the MB on the surface will be better, creating conditions for the oxidizing radicals to easily react with the colourant.

To better understand the shape, size and crystal formation of the Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO catalyst, we studied the transmission electron microscopy (TEM) images.

Figure 3 shows that the particle size of the Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO catalyst is larger than that of ZrO$_2$/CuO. According to the particle size distribution curves in
Figure 3c–d, ZrO$_2$/CuO concentrates around 20 nm, while Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO concentrates around 30 nm.

Figure 2. FE-SEM of x mol% Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO: (a) x = 2; (b) x = 4; (c) x = 6; (d) x = 8.

Figure 3. TEM and the particle size distribution curve of ZrO$_2$/CuO (a,c) and 2 mol% Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO (b,d).

3.3. Fourier Transform Infrared Spectroscopy and Energy Dispersive X-ray Spectroscopy of the Ce$^{3+}$/Ce$^{4+}$-Doped ZrO$_2$/CuO Nanocomposites

Figure 4 shows the FT-IR spectra of ZrO$_2$/CuO and Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO. The Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO materials all have absorption maximums around 3113–3153 cm$^{-1}$,
which is typical for the –OH group of wet water. The absorption peaks at 1710–1712 cm\(^{-1}\) and 1556–1566 cm\(^{-1}\) are characteristic of the vibrations of the Zr–O–H group in the material. In addition, the materials have an absorption maximum of 601–607 cm\(^{-1}\), which can be attributed to the vibrational stretching mode of the Cu-O bond. Bands at 424–524 cm\(^{-1}\) can be assigned to the Zr-O vibration mode in composites.

Figure 4. (a) FT-IR of x mol% Ce\(^{3+}\)/Ce\(^{4+}\)-doped ZrO\(_2\)/CuO (x = 0; 2; 4; 6), (b) EDS, (c) mapping imaging of 8 mol% Ce\(^{3+}\)/Ce\(^{4+}\)-doped ZrO\(_2\)/CuO.  

Figure 4b shows the presence of elements Ce, Zr, Cu and O, confirming the presence of Ce doping in ZrO\(_2\)/CuO nanocomposites. We performed EDS mapping, which is equipped with SEM. Figure 4c clearly show the uniform spread of Zr, Cu, O and Ce elements.

3.4. Nitrogen Adsorption-Desorption Isotherms of the Ce\(^{3+}\)/Ce\(^{4+}\)-Doped ZrO\(_2\)/CuO Nanocomposites

The specific surface areas of the Ce\(^{3+}\)/Ce\(^{4+}\)-doped ZrO\(_2\)/CuO and ZrO\(_2\)/CuO nanocomposites were determined by measuring the nitrogen adsorption-desorption isotherms, as shown in Figure 5. All of them are all type III adsorption isotherms [13]. The BET surface areas of ZrO\(_2\)/CuO and Ce\(^{3+}\)/Ce\(^{4+}\)-doped ZrO\(_2\)/CuO are 15.59 and 13.52 m\(^2\)g\(^{-1}\). The
large surface area of the catalyst facilitates the adsorption of the pigment to the surface of the material, thereby improving the photocatalyst efficiency.

![Figure 5](image1.png)

**Figure 5.** Nitrogen adsorption-desorption isotherms of (a) ZrO\(_2\)/CuO, and (b) 2 mol% Ce\(^{3+}\)/Ce\(^{4+}\)-doped ZrO\(_2\)/CuO.

### 3.5. UV-Vis Absorption Spectrum of Ce\(^{3+}\)/Ce\(^{4+}\)-Doped ZrO\(_2\)/CuO Nanocomposites

Figure 6 shows the UV-Vis absorption spectrum and the bandgap energy of the Ce\(^{3+}\)/Ce\(^{4+}\)-doped ZrO\(_2\)/CuO. The results show that the Ce\(^{3+}\)/Ce\(^{4+}\)-doped ZrO\(_2\)/CuO oxide composite material has an absorption region from UV to the visible region (200–1000 nm). To calculate the band gap, the Tauc relation is used:

\[
\alpha h \nu = A(h \nu - E_g)^n
\]  

where \(\alpha\) is the absorption coefficient, \(h\) is the Planck constant, \(\nu\) is the frequency of the incident photon, \(A\) is a constant that depends on the transition probability, \(E_g\) is the band gap energy and \(n\) is an index that depends on the transition probability of the nature of the electronic transition.

![Figure 6](image2.png)

**Figure 6.** (a) The UV-Vis DRS and (b) The Kubelka-Munk energy curve versus the band gap (eV) of the \(x\) mol% Ce\(^{3+}\)/Ce\(^{4+}\)-doped ZrO\(_2\)/CuO (\(x = 0; 2; 4; 6; 8\)).
The bandgap energy of Ce\(^{3+}/Ce^{4+}\)-doped ZrO\(_2/CuO\) was found to be in the range of 1.445–1.475 eV. When increasing the Ce\(^{3+}/Ce^{4+}\) doping concentration from 0 to 8 mol\%, the band gap increased slightly from 1.445 to 1.475 eV. When Ce was doped into ZrO\(_2/CuO\), the 5d and 6s orbitals of Ce overlapping with the d orbitals of Cu and Zr can increase the size of the valence band and also lower the position of its maximum, thereby increasing the band gap of mixed semiconductor oxide. The increase in the optical band gap upon Ce doping is similar to the increase in the band gap of Ag\(_2O\) upon Zn doping, as reported by De, Arup Kumar et al. [14]. The decrease in the band gap of the ZrO\(_2/CuO\) nanocomposites material compared with that of pure ZrO\(_2\) is mainly due to the introduction of CuO into the ZrO\(_2\) host matrix. It was found that when two metals combine, the band gap decreases and thus a shift to the visible region is observed [15].

The narrowing of the band gap can be attributed to the appearance of an impurity region (CuO) formed by overlapping impurity states and local states formed by the combination of Cu 2p and Zr 3p [7]. This result is similar to previous studies [16]. The photocatalytic reaction is initiated by the absorption of light with an energy equal to or greater than the band gap of the semiconductor. The band gap is in the range of 1.445–1.475 eV, so it is expected that the catalyst material can absorb visible light.

3.6. Photocatalytic Activity of Ce\(^{3+}/Ce^{4+}\)-Doped ZrO\(_2/CuO\) Nanocomposites

To investigate the adsorption balance, 20 mg of 8 mol\% Ce\(^{3+}/Ce^{4+}\)-doped ZrO\(_2/CuO\) was added into 30 mL of 10 mgL\(^{-1}\) MB solution. The suspension was stirred in the dark; samples were measured via UV-Vis spectroscopy. Figure 7 shows that after the first 30 min, the concentration of MB strongly decreased, then at 60 min slightly decreased, and at 90 min, the concentration of MB increased slightly (desorption). It is shown that after 60 min of adsorption, equilibration has occurred.

![Figure 7. UV-Vis spectrum of MB after being adsorbed by ZrO\(_2/CuO\)-doped 8 mol\% Ce\(^{3+}/Ce^{4+}\).](image)

Figure 8 shows the UV-Vis absorption spectrum of MB under visible light at different times in the presence of Ce\(^{3+}/Ce^{4+}\)-doped ZrO\(_2/CuO\). The evolution of MB photodegradation was monitored by measuring the absorbance at the wavelength of about \(\lambda = 662\) nm at different times. The maximum absorption peaks of MB gradually decreased and almost disappeared in 180 min of illumination.
Figure 8. UV-Vis absorbance of MB under visible light at different times in the presence of x mol% Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO: (a) $x = 0$; (b) $x = 2$; (c) $x = 4$; (d) $x = 6$; (e) $x = 8$.

The reactions that occur during photocatalysis are described below. The reaction begins by generating excitons on the metal oxide surface (MeO) [17]:

$$\text{MeO} + h\nu \rightarrow \text{MeO} (h^+ + e^-)$$

Oxidation reactions due to the photocatalytic effect:

$$h^+ + \text{H}_2\text{O} \rightarrow \text{H}^+ + \bullet\text{OH}$$

$$2h^+ + 2\text{H}_2\text{O} \rightarrow 2\text{H}^+ + \text{H}_2\text{O}_2$$

$$\text{H}_2\text{O}_2 \rightarrow 2 \bullet\text{OH}$$
Reduction reaction due to the photocatalytic effect:

\[ \text{e}^- + \text{O}_2 \rightarrow \bullet\text{O}_2^- \]

\[ \bullet\text{O}_2^- + \text{H}_2\text{O} + \text{H}^+ \rightarrow \text{H}_2\text{O}_2 + \text{O}_2 \]

\[ \text{H}_2\text{O}_2 \rightarrow 2\bullet\text{OH} \]

\[ \bullet\text{OH} + \text{Dye} \rightarrow \text{Degradation} \]

\[ \bullet\text{O}_2^- + \text{Dye} \rightarrow \text{Degradation} \]

Figure 9a shows the ZrO$_2$/CuO catalyst, the photocatalytic efficiency of MB decomposition by Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO increased significantly. The Ce$^{3+}$/Ce$^{4+}$ doping concentration increased, and the photocatalytic efficiency under visible light also increased. Although the $E_g$ values of ZrO$_2$/CuO and ZrO$_2$/CuO-doped Ce$^{3+}$/Ce$^{4+}$ were not significantly different, the results showed that the photocatalytic degradation efficiency was enhanced by Ce$^{3+}$/Ce$^{4+}$ doping. This could be due to the fact that as the Ce$^{3+}$/Ce$^{4+}$ ion concentration increases, an increase in oxygen vacancy defects in the crystal lattice occurs. This leads to the redox pair Ce$^{3+}$/Ce$^{4+}$ being capable of shifting between Ce$_2$O$_3$ and CeO$_2$, which reduces electron-hole recombination [18].

Figure 9. (a) Photodegradation of MB, (b) the reaction rate constant k of the MB degradation in the presence of x mol% Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO ($x = 0; 2; 4; 6; 8$), (c) reuse of 8 mol% of Ce$^{3+}$/Ce$^{4+}$ doping ZrO$_2$/CuO.
The MB degradation processes all show first-order kinetics by plotting ln(C/C₀) versus irradiation time, t. The apparent response rate constant (k_{app}) was calculated from the slope of the curve, as illustrated in Figure 9b. The k_{app} value continuously increased as the Ce³⁺/Ce⁴⁺ doping concentration increased, with x = 0, k_{app} = 0.0074 min⁻¹; x = 2, k_{app} = 0.0093 min⁻¹; x = 4, k_{app} = 0.0122 min⁻¹; x = 6, k_{app} = 0.0123 min⁻¹; and x = 8, k_{app} = 0.0138 min⁻¹. It was shown that 8 mol% Ce³⁺/Ce⁴⁺-doped ZrO₂/CuO exhibited the highest k_{app} = 0.0138 min⁻¹, much higher than that of undoped ZrO₂/CuO with Ce³⁺/Ce⁴⁺.

Figure 9c shows the stability of the Ce³⁺/Ce⁴⁺-doped ZrO₂/CuO nanocomposites. The stability of the MOS material was evaluated by performing photocatalyst recycling experiments for a duration of 180 min. The activity was found to be roughly the same in the two repeated runs, and then there was a slight decrease in the third and fourth runs.

We assume that there is metal-to-metal charge transfer (MMCT). The MMCT effect is assumed to be: Zr⁴⁺–O–Ce⁴⁺ to Zr⁴⁺–O–Ce³⁺ and Zr⁴⁺–O–Cu²⁺ to Zr⁴⁺–O–Cu⁺. The effect is when two different metals in the mixture form an oxygen bridge, which helps electrons and holes move efficiently and avoid recombination, increasing the photocatalytic efficiency of the Ce³⁺/Ce⁴⁺-doped ZrO₂/CuO catalyst [19]. Furthermore, Ce³⁺/Ce⁴⁺ ions act as electron-trapping sites reducing charge-pair recombination and thus enhancing photocatalytic activity [20,21].

Table 1 shows the photocatalytic degradation of MB using the various heterojunction photocatalyst. It shows that the combination of semiconductor oxides, or metal ion doping, shows an improved rate constant compared to single semiconductor oxides.

| Photocatalyst          | Synthesis Method | Light Source | Rate Constant (min⁻¹) | Reference |
|------------------------|------------------|--------------|------------------------|-----------|
| Fe₂O₃/graphene/CuO     | Solvothermal     | Visible      | 72.5 × 10⁻³            | [22]      |
| CuO/ZnO               | Impregnation     | UV lamp      | 182 × 10⁻³             | [23]      |
| ZrO₂/AgCl:Eu³⁺        | Sol-gel          | Visible      | 14 × 10⁻³              | [24]      |
| C-doped ZrO₂          | Sol-gel          | UVC lamp     | 7.3 × 10⁻³             | [25]      |
| N-TiO₂/ZrO₂           | Hydrothermal     | UV light     | 29 × 10⁻³              | [26]      |
| ZrO₂/CuO              | Combustion       | Visible      | 11.19 × 10⁻³           | [6]       |
| GO-ZrO₂               | Co-precipitation | Visible      | 57.5 × 10⁻³            | [27]      |
| CeO₂                  | Precipitation    | UV light     | 12.1 × 10⁻³            | [28]      |
| V₂O₅-CeO₂             | Precipitation    | Visible      | 108 × 10⁻³             | [29]      |
| CeO₂/TiO₂             | Precipitation    | Visible      | 34 × 10⁻³              | [30]      |
| Ce³⁺/Ce⁴⁺-doped ZrO₂/CuO | Hydrothermal     | Visible      | 13.8 × 10⁻³          | This work |

The ZrO₂/CuO-doped Ce³⁺/Ce⁴⁺ photocatalyst can be reproducible and without destruction. This reproducible process can be confirmed by FT-IR, as shown in Figure 10. It is clear that the characteristic bands of MB, which are at 1383, 1324, 1245, 884 and 670 cm⁻¹, appear after adsorbing [31], while they disappear after 180 min of irradiation. Combined with the results of photocatalytic reuse experiments, it is proven that the Ce³⁺/Ce⁴⁺-doped ZrO₂/CuO nanocomposites have stability.
Figure 10. FT-IR spectrum of (a) MB, (b) MB adsorbed onto Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO before irradiation, (c) MB adsorbed on Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO 180 min after irradiation.

4. Conclusions

Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO nanocomposites have been synthesized by the simple hydrothermal method. The obtained material is a mixed semiconductor oxide ZrO$_2$ and CuO. The coupling between CuO and ZrO$_2$ oxides has shown that the light absorption capacity is extended from UV to the visible region. Photocatalytic activity is enhanced when doping Ce$^{3+}$/Ce$^{4+}$ ions because Ce$^{3+}$/Ce$^{4+}$ ions have higher separation efficiency of charge carriers, which reduces electron-hole recombination. The Ce$^{3+}$/Ce$^{4+}$-doped ZrO$_2$/CuO nanocomposites showed significantly improved photocatalytic activity. High photocatalysis activity with 94.5% degradation efficiency of MB was achieved after 180 min under visible light irradiation. It is believed that these materials will have promising applications in the wastewater treatment field.

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