Effects of Adding Alkali Metals and Organic Cations to Cu-Based Perovskite Solar Cells

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Abstract: First-principles electronic band calculations were used to investigate the effects of alkali metals and organic cations added to Cu-based perovskite solar cells. The copper d-orbital band was slightly above the valence-band maximum and functioned as an acceptor level for carrier generation. Excitation from iodine p-orbitals and copper d-orbitals to alkali metal s-orbitals could suppress carrier recombination and promote carrier transport. Experimental solar conversion efficiencies increased after adding both Cu and Na, in agreement with the calculations. Total-energy calculations indicated that the perovskite crystal stability increased with the addition of ethyl ammonium, although the total energy decreased with the addition of Cu and Na.

Keywords: copper; sodium; ethyl ammonium; first-principles calculations; perovskite; solar cell

1. Introduction

There have been many efforts to improve the conversion efficiencies and durabilities of perovskite photovoltaic devices by adding metal, halogen, and organic ions to the precursor solutions [1–3]. Other approaches have included the development of scalable processes via electrodeposition [4,5], stable fully inorganic perovskites [6], polymer composites using perovskites [7], and solvent effects in the precursor solution on perovskite film microstructures [8].

Here, additives such as copper (Cu), sodium (Na), and ethyl ammonium (EA) were examined. Cu compounds such as copper thiocyanate (CuSCN), copper oxides, (CuO), and copper iodide, were mainly used as hole-transport materials that replaced organic versions [9–14]. Although there have been many reports on the addition of alkali metals to perovskite precursor solutions [15–23], relatively few reported on the addition of Cu [24–27]. The addition of CuBr2 and NaCl to the solutions improved the solar conversion efficiency and device durability [28–30]. In those studies, lattice distortion in the perovskite crystals was reduced by small amounts of Cu, and lattice defects were suppressed with Na at the defect sites after desorption of methylammonium (MA), which improved conversion efficiency and device durability.

First-principles calculations of perovskite crystals have been performed using structural models in which organic cations, metal cations, and halogen anions were replaced with other groups to examine the crystal structure stability. CH3NH3PbI3 (MAPbI3) is the standard perovskite compound used for photoelectric conversion [31]. Previously, calculations indicated that EA substitution for MA enhanced the structural stability [32], and the calculated energy gap agreed well with experimental values [33]. The addition of other organic cations and combinations of multiple organic cations have also been studied. The introduction of EA and butyl-ammonium affected the conduction-band minima,
valence-band maxima, and the surface morphologies of MA-based perovskites [34]. Increased coulomb interactions between cations, attributed to the additional organic cations, enhanced the perovskite stability and device durability. There have been other reports on using larger organic cations to replace MA and improve device properties [35–39].

The effects of halogen additions have been examined computationally and experimentally [40–43]. A Br-rich sample resulted in larger grain sizes and fewer grain boundaries because of the reduced number of nucleation sites during perovskite crystal growth [44]. Defects distributed at grain boundaries were thus reduced by fewer boundaries, which increased carrier lifetimes. Br-rich samples exhibited higher thermal and optical stabilities relative to MAPbI$_3$ devices. It is expected that perovskite film quality and stability could be improved via halogen selectivity. The replacement of I with Br or Cl changed the band gap and charge-transfer properties. Monovalent pseudo-halogen, such as thiocyanate, have properties like those of halogens, they could improve photovoltaic conversion and stability, and may prevent oxidation of Sn$^{2+}$ to Sn$^{4+}$ in Sn-based perovskites [45]. The latter was expected to suppress oxidation-induced degradation. The thiocyanate ions also increased the grain size and improved the surface morphology and crystallinity, which increased photoelectric conversion and stability. Thus, the Pb, MA, and halogen sites are very important because the perovskite energy gap and crystallinity change with added materials.

Here, the effects of adding Cu, Na, and EA to the perovskite precursor solution were investigated with first-principles calculations. The addition of 2% Cu and 2% Na to MAPbI$_3$ improved the photoelectric conversion efficiency [29]. Therefore, increased conversion properties and device durability by adding EA, together with 2% Cu and 2% Na, were examined. The calculations were performed to understand the doping effects in more detail, and to compare them with experimental results. Both total- and partial-substitution structure models approximating perovskite compositions in actual devices were used to investigate the effects.

2. Computational Conditions and Experimental Methods

The electronic structures of the perovskite crystals were single-point-calculated with crystallographic structural data obtained from X-ray diffraction. The ab initio quantum calculations were performed using the Vanderbilt ultrasoft pseudo-potentials, scalar relativistic generalized gradient approximations and the Perdew–Burke–Ernzerhof exchange correlation functional and density functional theory without consideration of spin–orbital coupling effect (Quantum Espresso Software Ver. 5. 2. 1, Quantum ESPRESSO Foundation, Cambridge, UK). The basis functions were used properly according to the cases of itinerant and localized electron system. Plane-wave basis set cut offs for the wave functions and charge density were set at 25 and 225 Rydberg. Plane-wave basis set cut offs for the wave functions and charge density were set at 25 and 225 Rydberg. The perovskite crystals were constructed with a crystal system of $P\overline{4}m3m$. Uniform k-point grid (4×4×4) in the Brillouin zone was used to calculate the electronic structure and partial density of state. The ABX$_3$ ($A = Na^+, K^+, Rb^+, Cs^+, MA^+$, or EA$^+$, $B = Pb^{2+}$ or Cu$^{2+}$, $X = I^-$, Br$^-$, or Cl$^-$) perovskite crystals were formed as a cubic system with a $1 \times 1 \times 1$ single cell. The cation of MA$^+$, EA$^+$, Na$^+$, K$^+$, Rb$^+$, or Cs$^+$ was set in the center position of the unit cell ($1 \times 1 \times 1$). The cation of Pb$^{2+}$ or Cu$^{2+}$ ion was set at the position of $\Gamma \ (0, 0, 0)$. As the Cu-incorporated perovskite crystal modelling with $2 \times 2 \times 2$ supercells, parts of the Pb atom at the B-sites were substituted with Cu ion for one-atom substitution at the center of the cubic structure. The Cu-incorporated ABX$_3$ ($A = MA^+, EA^+$, or Na$^+$, $X = I^-$ or Br$^-$) perovskite crystals were constructed with the $2 \times 2 \times 2$ supercells, and were used for the band calculation. The band structures, effective mass and band gap were analyzed for the Brillouin zone of the lattice of the perovskite crystals along the direction of wave vector. Path for ABX$_3$ perovskite crystal were set as follows, $\Gamma \ (0, 0, 0) \rightarrow X \ (0, \frac{1}{2}, 0) \rightarrow M \ (1/2, 1/2, 0) \rightarrow \Gamma \rightarrow R \ (1/2, 1/2, 1/2) \rightarrow X$, $M \rightarrow R$. The Fermi energy was set at zero. The density of states (DOS) and partial density of states (pDOS) were calculated to make clear the energy level for each orbital near the valence band (VB) and conduction band (CB). Structural optimization was performed for the structural models containing the alkali metals. The cut-off energy of the planar wave-
function was set to 80 eV for the structural optimization and it was set to 25 eV for the other calculations. A $4 \times 4 \times 4$ $k$-point mesh was used for calculations of all structures [46–48].

F-doped tin oxide (FTO) substrates were cleaned in an ultrasonic bath with acetone and methanol and dried under nitrogen gas. The TiO$_2$ (0.15 and 0.30 M) precursor solutions were prepared from titanium diisopropoxide bis(acetyl acetonate) (Sigma-Aldrich, Tokyo, Japan, 0.055 and 0.11 mL) with 1-butanol (1 mL). The 0.15 M TiO$_2$ precursor solution was spin-coated on the FTO substrate at 3000 rpm for 30 s, and the coated substrate was then annealed at 125 °C for 5 min. The 0.30 M TiO$_2$ precursor solution was spin-coated on the TiO$_2$ layer at 3000 rpm for 30 s, and the resulting substrate was annealed at 125 °C for 5 min. The process to form the 0.30 M precursor layer was performed twice. Then, the FTO substrate was sintered at 550 °C for 30 min to form a compact TiO$_2$ layer. To form the mesoporous TiO$_2$ layer, a TiO$_2$ paste was prepared from the TiO$_2$ powder (Aerosil, Tokyo, Japan, P-25, 200 mg) with poly(ethylene glycol) (Nacalai Tesque, Kyoto, Japan, PEG #20000, 20 mg) in ultrapure water [49]. The solution was mixed with acetylacetone (Fujifilm Wako Pure Chemical Corporation, Osaka, Japan, 20 mL) and surfactant (Sigma-Aldrich, Tokyo, Japan, Triton X-100, 10 mL) for 30 min. Then, the TiO$_2$ paste was spin-coated on the compact TiO$_2$ layer at 5000 rpm for 30 s. The resulting cell was annealed at 550 °C for 30 min to form the mesoporous TiO$_2$ layer.

To prepare the perovskite compounds, mixed solutions of CH$_3$NH$_3$I (2.4 M, Showa Chemical, Tokyo, Japan) and PbCl$_2$ (0.8 M, Sigma-Aldrich, St. Louis, MO, USA) in N,N-dimethylformamide (DMF, Sigma-Aldrich, 0.5 mL) were prepared for the standard cell. Pb or MA in the perovskite structure was expected to be substituted by Cu, Na or EA, respectively. These perovskite solutions were then introduced into the TiO$_2$ mesopores by spin-coating at 2000 rpm for 60 s, which is followed by annealing in air. During the spin-coating, a hot air-blowing method was applied [50]. Temperatures of the cells during the air-blowing were set at 90 °C. A polysilane solution was prepared by mixing chlorobenzene (Fujifilm Wako Pure Chemical Corporation, 0.5 mL) with decaphenylcyclopentasilane (DPPS, Osaka Gas Chemicals, Osaka, Japan, OGSOL SI-30-15, 10 mg). During the last 15 s of the third spin-coating of the perovskite precursor solutions, the DPPS polysilane solution was also spin-coated on the perovskite layer [51–54]. After the spin-coating, the thin films were annealed from 90 to 160 °C in steps of 10 °C, holding each temperature for 10 min [55]. The temperature rising rate is ~5 °C min$^{-1}$, which was not included in the annealing time.

A hole-transport layer was prepared by spin-coating. A solution of spiro-OMeTAD (Fujifilm Wako Pure Chemical Corporation, Osaka, Japan, 36.1 mg) in chlorobenzene (Fujifilm Wako Pure Chemical Corporation, 0.5 mL) was mixed with a solution of lithium bis(trifluoromethylsulfonyl)imide (Li-TFSI, Tokyo Chemical Industry, Tokyo, Japan, 260 mg) in acetonitrile (Nacalai Tesque, Kyoto, Japan, 0.5 mL) and tris(2-(1H-pyrazol-1-yl)-4-tert-butyl pyridine)cobalt(III) tri[bis(trifluoromethane)sulfonimide] (FK209, Sigma-Aldrich, 188 mg) in acetonitrile (0.5 mL) for 24 h. The former solution with 4-tertbutylpyridine (Sigma-Aldrich, 0.018 mL) was mixed with the Li-TFSI solution (0.010 mL) and FK209 solution (0.004 mL) for 30 min at 70 °C. Then, the spiro-OMeTAD solution was spin-coated on the perovskite layer at 4000 rpm for 30 s. All procedures were performed in ambient air. Finally, gold (Au) electrodes were evaporated as top electrodes using a metal mask for the patterning.

3. Results and Discussion

First-principles calculated band structures and partial density of states are shown in Figure 1; parameters are listed in Table 1. Figure 1a–d shows the effects of halogen substitution. For MAPbI$_3$, the energy gap increased when I was replaced with Br or Cl. An increase in the energy gap would increase the open-circuit voltage. Both the effective mass ratio of electrons, in the case of total Br substitution, and that of holes, in the case of total Cl substitution, increased relative to those values for MAPbI$_3$. Because of the inverse relationship between effective mass and carrier mobility, it was expected that carrier mobilities would decrease when Br or Cl was added. However, for the three
halogens in MAPbClBrI in Figure 1d, the effective mass ratios of the carriers were not significantly different from those of MAPbI$_3$, and the energy gap increased.

Table 1 shows the total energy per unit cell of the structure model; a small value indicates a more stable crystal structure. Therefore, because the total energy decreased by replacing I with Br or Cl, the crystal structure was expected to be more stable.

| Compound    | Total Energy (keV) | Energy Gap (eV) | $m_e*/m_0$ | $m_h*/m_0$ |
|-------------|--------------------|-----------------|------------|------------|
| MAPbI$_3$   | −3.50              | 1.51            | 0.071      | 0.100      |
| MAPbBr$_3$  | −3.66              | 2.26            | 0.224      | 0.100      |
| MAPbCl$_3$  | −3.78              | 2.75            | 0.144      | 0.462      |
| MAPbClBrI   | −3.64              | 2.03            | 0.092      | 0.102      |
| MACuI$_3$   | −2.52              | 1.48            | 0.136      | 0.079      |

Figure 2a–c shows the calculated results when the organic and metal cations were replaced with EA and Cu. The horizontal axis of the figure represents the wavenumber vector, and each symbol represents a symmetry point in reciprocal lattice space, as follows: $\Gamma$ (0, 0, 0), $X$ (0, 1/2, 0), $M$ (1/2, 1/2, 0), and $R$ (1/2, 1/2, 1/2). The addition of EA increased the crystal stability, in good agreement with previous studies [30]. When Pb was replaced by Cu, the hole mobility was expected to increase. However, the crystal stability would decrease. For EACuI$_3$ in Figure 1c, the total energy was lower than that of MACuI$_3$, indicating structure stabilization by EA substitution in the presence of Cu.
Table 1. Calculated parameters of various perovskite compounds.

| Compound       | Total Energy (keV) | Energy Gap (eV) | $m_e^*/m_0$ | $m_h^*/m_0$ |
|-----------------|--------------------|-----------------|-------------|-------------|
| MAPbI$_3$       | −3.50              | 1.51            | 0.071       | 0.100       |
| MAPbBr$_3$      | −3.66              | 2.26            | 0.224       | 0.100       |
| MAPbCl$_3$      | −3.78              | 2.75            | 0.144       | 0.462       |
| MAPbClBrI       | −3.64              | 2.03            | 0.092       | 0.102       |
| MACuI$_3$       | −2.52              | 1.48            | 0.136       | 0.079       |
| EAPbI$_3$       | −3.68              | 1.43            | 0.076       | 0.104       |
| EACuI$_3$       | −2.71              | 1.42            | 0.097       | 0.080       |
| NaPbI$_3$       | −2.99              | 1.06            | 0.077       | 0.062       |
| KPbI$_3$        | −3.00              | 1.04            | 0.068       | 0.062       |
| RbPbI$_3$       | −3.00              | 1.03            | 0.067       | 0.062       |
| CsPbI$_3$       | −3.00              | 1.00            | 0.067       | 0.061       |

Figure 2a–c shows the calculated results when the organic and metal cations were replaced with EA and Cu. The horizontal axis of the figure represents the wavenumber vector, and each symbol represents a symmetry point in reciprocal lattice space, as follows: Г (0, 0, 0), X (0, 1/2, 0), M (1/2, 1/2, 0), and R (1/2, 1/2, 1/2). The addition of EA increased the crystal stability, in good agreement with previous studies [30]. When Pb was replaced by Cu, the hole mobility was expected to increase. However, the crystal stability would decrease. For EACuI$_3$ in Figure 1c, the total energy was lower than that of MACuI$_3$, indicating structure stabilization by EA substitution in the presence of Cu.

Figure 2. Calculated band structures and DOS of (a) MACuI$_3$, (b) EAPbI$_3$, and (c) EACuI$_3$.

Figure 3a–d shows the calculated results when the organic cation was replaced by an alkali metal. Although there were no significant differences in the resulting parameters, there was a difference in the energy level of the alkali–metal band that was formed slightly above the conduction band minimum.
Figure 3. Calculated band structures and DOS of (a) NaPbI₃, (b) KPbI₃, (c) RbPbI₃ and (d) CsPbI₃.

The calculated band structures and partial density of states of the partial-substitution structure models are shown in Figure 4. These models contained more atoms than the total-substitution structure models, and thus required more time for the band calculations. In contrast to Figure 4a, where one of the eight MA molecules was replaced with EA, the addition of Cu resulted in the formation of a shallow band of Cu d-orbitals slightly above the band of I p-orbitals. This decreased the energy gap and hole mobility. Furthermore, comparing Figure 4b,c, the partial substitution of Na for some of the MA resulted in a band of Na s-orbitals slightly above the conduction band minimum and a slight increase in electron mobility. In Figure 4d, the energy gap was increased by substituting some of the I with Br, which was in good agreement with the calculated results for the total-substitution structure model. An increased effective mass for holes was attributed to 3d-orbital localization, as shown in Table 2.
Figure 4. Calculated band structures and DOS of (a) MA$_{0.875}$EA$_{0.125}$PbI$_3$, (b) MA$_{0.875}$EA$_{0.125}$Pb$_{0.875}$Cu$_{0.125}$I$_3$, (c) MA$_{0.750}$EA$_{0.125}$Na$_{0.125}$Pb$_{0.875}$Cu$_{0.125}$I$_3$ and (d) MA$_{0.750}$EA$_{0.125}$Na$_{0.125}$Pb$_{0.875}$Cu$_{0.125}$I$_3$Br$_{0.75}$.

Table 2. Calculated parameters of partially substituted perovskite compounds.

| Compound                                      | Total Energy (keV) | Energy Gap (eV) | $m_e^*/m_0$ | $m_h^*/m_0$ |
|-----------------------------------------------|--------------------|----------------|-------------|-------------|
| MA$_{0.875}$EA$_{0.125}$PbI$_3$                | −3.52              | 1.49           | 0.228       | 0.199       |
| MA$_{0.875}$EA$_{0.125}$Pb$_{0.875}$Cu$_{0.125}$I$_3$ | −3.39              | 1.00           | 0.266       | 0.352       |
| MA$_{0.750}$EA$_{0.125}$Na$_{0.125}$Pb$_{0.875}$Cu$_{0.125}$I$_3$ | −3.32              | 1.04           | 0.241       | 0.355       |
| MA$_{0.750}$EA$_{0.125}$Na$_{0.125}$Pb$_{0.875}$Cu$_{0.125}$I$_3$Br$_{0.75}$ | −3.36              | 1.30           | 0.250       | 0.490       |

Figure 5 shows experimental current–voltage curves obtained from perovskite photovoltaic devices. Detailed parameters in Table 3 indicated the effects of additives on device performances. From the calculated results on the partial substitution structure models in Figure 4, it was expected that the addition of Cu would decrease the energy gap and reduce hole mobility. However, the results in Table 3 indicated that co-addition of Cu and Na slightly increased the energy gap, the short-circuit current density ($J_{SC}$), the open-circuit voltage ($V_{OC}$), and the fill factor ($FF$), resulting in a higher conversion efficiency. Figure 1a,b shows that the energy gap increased when I was replaced by Br, and the $V_{OC}$ enhancement from the increased energy gap could be considered an effect of Br addition. The reason for the slight $J_{SC}$ increase was attributed to increased carrier generation resulting from the acceptor-level Cu d-orbital band. The additional excitations from the Cu d-orbital to the Na s-orbital would also promote carrier generation.
Figure 5. J-V characteristics of the present perovskite solar cells.

Table 3. Measured device parameters of perovskite solar cells.

| Devices                | $J_{SC}$ (mA cm$^{-2}$) | $V_{OC}$ (V) | $FF$ | $R_S$ (Ω cm$^2$) | $R_{Sh}$ (Ω cm$^2$) | $\eta$ (%) | $\eta_{ave}$ (%) | $E_g$ |
|------------------------|--------------------------|--------------|------|------------------|---------------------|------------|------------------|-------|
| Standard               | 22.2                     | 0.739        | 0.497| 4.18             | 383                 | 8.17       | 5.82             | 1.55  |
| Cu 2% + Na 2%          | 21.7                     | 0.841        | 0.578| 5.93             | 594                 | 10.5       | 8.36             | 1.56  |
| Cu 2% + Na 2% + EA 2.5%| 20.0                     | 0.811        | 0.559| 6.55             | 604                 | 9.08       | 7.20             | 1.56  |
| Cu 2% + Na 2% + EA 5%  | 21.3                     | 0.843        | 0.585| 5.12             | 558                 | 10.5       | 8.67             | 1.57  |
| Cu 2% + Na 2% + EA 10% | 16.1                     | 0.824        | 0.586| 5.29             | 445                 | 7.78       | 5.77             | 1.57  |

Previously [29], the co-addition of 2% Cu and 2% Na exhibited the highest conversion efficiency. When the amount of EA was varied, in addition to 2% Cu and 2% Na, the highest conversion efficiency was obtained with 5% EA. For the device with the lowest amount of EABr, the effect of increasing the energy gap and $V_{OC}$ was small because of the low bromine content. A comparatively small value of $J_{SC}$ was obtained for the device with the highest amount of EABr. In Table 1, the calculated effective mass ratio for the electrons increased when I was replaced with Br. Hence, the electron mobility decreased with the addition of Br, decreasing $J_{SC}$. The devices doped with Cu-Na and Cu-Na-EA exhibited the same conversion efficiencies. From the density of states in Figure 2b, no peaks corresponding to C or N were observed near the conduction-band minimum or the valence-band maximum. Thus, the substitution of MA with EA was estimated to have no special effect on the electronic structures. Furthermore, because there was almost no difference in the effective mass ratios of carriers between MAPbI$_3$ and EAPbI$_3$ (Table 1), the two devices had similar conversion efficiencies. However, there was a difference in the durability of the devices. The conversion efficiency of the device doped with Cu and Na decreased to 79.1% of the initial value after four weeks, while that of the device containing 2% Cu, 2% Na, and 5% EABr remained at 96.2% of its initial value. The total-energy calculation results in Table 1 indicate that the crystal structure was destabilized when Pb and MA were replaced with Cu and Na, respectively. The devices with Cu, Na, and EA exhibited higher durabilities than devices with just Cu and Na, which confirmed that the addition of EA stabilized the crystal structure. Therefore, the addition of organic cations more stable than MA to Cu-based perovskites enhanced the durability. It was also expected...
that the device durability was highly dependent on the stability of the perovskite crystal, and that the durability could be estimated by the calculated total energy.

Figure 6 shows X-ray diffraction (XRD) measurements for the MAPbI\textsubscript{3} device and those doped with Cu, Na, and EA. Table 4 shows the measured structural parameters calculated from the XRD data. A diffraction peak corresponding to tetragonal (211) planes was observed at 23.5°. The peak intensity was slightly lower in the doped devices relative to that for MAPbI\textsubscript{3}, suggesting that elimination of lattice distortion by the substitution of Pb with Cu reduced the peak intensity. Although the ionic radii of Cu and Na are smaller than those of Pb and MA, their additions increased the lattice constant. The crystal lattice was expanded by the presence of Na in the interstitial position relative to that of MA. The lattice constants of devices doped with Cu, Na, and EA were the smallest, because of I substitution with Br, which had a smaller ionic radius. Crystallites of MAPbI\textsubscript{3} were larger than those of the doped devices. Previously, CuBr\textsubscript{2} addition to the perovskite precursor solution slowed the crystallization rate of the perovskite film, and decreased the crystallite size and diffraction-peak intensity. During annealing of the perovskite film, the color-changing rates with added Cu and Na were slower than those of MAPbI\textsubscript{3}, indicating that the addition of CuBr\textsubscript{2} decreased the crystallization rate.

Figure 7 shows optical microscopy images of perovskite crystals in actual devices. In MAPbI\textsubscript{3} (Figure 7a), the surface morphology was non-uniform with less coverage. The addition of Cu and Na significantly increased the surface coverage and the homogeneity, as observed in Figure 7b. This suggests that the addition of CuBr\textsubscript{2} reduced the crystallization rate, which, combined with the gradual increase of the annealing temperature, contributed to the formation of a homogeneous film. The densest and most homogeneous perovskite films were obtained for devices doped with Cu, Na, and EA, as observed in Figure 7c. The increased crystallization with the added EA enhanced the surface morphology.

![Figure 6. XRD patterns of the present perovskite solar cells.](image-url)

Table 4. Measured structural parameters of perovskite crystals.

| Devices       | $I_{100}/I_{210}$ | Lattice Constant (Å) | Crystallite Size (Å) |
|---------------|-------------------|-----------------------|----------------------|
| Standard      | 8.7               | 6.262 (1)             | 697                  |
| CuBr\textsubscript{2} 2% NaBr 2% | 2.6               | 6.271 (1)             | 679                  |
| Cu Na 2% EABr 5% | 3.1               | 6.261(1)              | 674                  |
The valence band maximum increased in the order Na, K, Rb, and Cs, which indicated that perovskite solar cells.

In Figure 3a–d, the alkali-metal energy bands formed above the conduction band minimum varied with the metal. These results are summarized in Figure 9a, and an enlarged view of the red rectangle is shown in Figure 9b. Substitution of MA with alkali metals significantly decreased the energy gap in the order Na, K, Rb, and Cs. Because the alkali-metal additions in the actual devices were a few mol%, the energy gaps were not expected to decrease as much as in the calculated results for the total-substitution models. The valence band maximum increased in the order Na, K, Rb, and Cs, which indicated that the addition of Rb or Cs increased the absorption of shorter-wavelength light in the visible region. The differences in energy levels in Figure 9b corresponded to energies that were higher than those of visible light. However, because the Cu d-orbital bands were formed at the valence band maximum by adding Cu, the difference in energy levels between the alkali-metal bands and the Cu bands was approximately the same energy as that in the visible-light region.
Figure 9. (a) Changes of band structures for various alkali metals. (b) Enlarged view at the band gap.

4. Conclusions

In summary, the effects of Cu, Na, and EA co-addition to MAPbI₃ perovskite crystals were investigated with first-principles calculations and experimental devices. The calculations indicated that substitution of all the I with Br or Cl increased the energy gap and increased $V_{OC}$. These additives to the perovskite precursor solution also increased the energy gap and $V_{OC}$ in all the devices relative to those of MAPbI₃. When some of the Pb was replaced with Cu, a shallow band of Cu d-orbitals formed slightly above the valence band maximum, which decreased the energy gap and reduced hole mobility. When a small amount of Cu was added to actual devices, the conversion efficiency and the energy gap increased slightly, which indicated that Cu energy levels formed in the forbidden band and functioned as acceptor levels. The excitation of electrons from the I p-orbitals to the Cu d-orbitals generated carriers, increasing $J_{SC}$. The alkali-metal energy bands formed above the conduction band minimum, which differed for the various alkali metals. Another possible reason for the increased $J_{SC}$ was the reduced loss of generated carriers by excitations from the Cu d-orbitals and the I p-orbitals to the s-orbitals of the alkali metals. The total-energy calculations indicated that the substitution of Pb and MA with Cu and Na, respectively, destabilized the crystal structure. When MA was replaced with EA, the crystal structure was stabilized. Thus, the addition of EA to the Cu and Na systems increased structural stability. The actual device doped with Cu, Na, and EA exhibited higher durability than that device doped with only Cu and Na. Therefore, crystal stabilization by EA addition occurred, even when Cu and Na were also added. Furthermore, the durability of the devices was highly dependent on the stability of the perovskite crystals, which could be estimated by the calculated total energies. Overall, it is expected that the photoelectric conversion and durability of Cu-based perovskite solar cells could be enhanced by adding various halogens or introducing more-stable organic cations.

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