Solar prominence diagnostics from non-LTE modelling of Mg II \(h\&k\) line profiles

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**ABSTRACT**

**Aims.** We investigate a new method to for obtaining the plasma parameters of solar prominences observed in the Mg II \(h\&k\) spectral lines by comparing line profiles from the IRIS satellite to a bank of profiles computed with a one-dimensional non-local thermodynamic equilibrium (non-LTE) radiative transfer code.

**Methods.** Using a grid of 1007 one-dimensional non-LTE radiative transfer models, some including a prominence-corona transition region (PCTR), we carry out this new method to match computed spectra to observed line profiles while accounting for line shift not present in the models. The prominence observations were carried out by the IRIS satellite on 19 April 2018.

**Results.** The prominence is very dynamic with many flows, including a large arm extending from the main body seen near the end of the observation. This flow is found to be redshifted, as is the prominence overall. The models are able to recover satisfactory matches in areas of the prominence where single line profiles are observed. We recover: mean temperatures of 6000–50 000 K; mean pressures of 0.01–0.5 dyne cm\(^{-2}\); column masses of 3.7 \(\times 10^{-8}–5 \times 10^{-4}\) g cm\(^{-2}\); a mean electron density of 7.3 \(\times 10^{6}–1.8 \times 10^{11}\) cm\(^{-3}\); and an ionisation degree \(n_{\text{ion}}/n_{\text{eq}} = 0.03–4500\). The highest values for the ionisation degree are found in areas where the line of sight crosses mostly plasma from the PCTR, correlating with high mean temperatures and correspondingly no H\(_{\alpha}\) emission.

**Conclusions.** This new method naturally returns information on how closely the observed and computed profiles match, allowing the user to identify areas where no satisfactory match between models and observations can be obtained. The inclusion of the PCTR was found to be important when fitting models to data as regions where satisfactory fits were found were more likely to contain a model encompassing a PCTR. The line core shift can also be recovered from this new method, and it shows a good qualitative match with that of the line core shift found by the quantile method. This demonstrates the effectiveness of the approach to line core shifts in the new method.

**Key words.** Sun: filaments, prominences – Sun: chromosphere – Sun: UV radiation

1. Introduction

Solar prominences, filaments when viewed on disc, are structures in the solar corona comprising of relatively cool and dense plasma. They form in filament channels, which manifest above the polarity inversion lines seen in photospheric magnetograms, suspended in dips in the magnetic field (Labrosse et al. 2010; Mackay et al. 2010; Vial & Engvold 2015). The high spatial and temporal resolution of space-based observations opens a new era of study into the dynamics, evolution, and structure of solar prominences. These properties are key to our understanding of prominence physics.

Since the launch of the Solar Dynamics Observatory (SDO; Pesnell et al. 2012), studies of extreme ultraviolet (EUV) prominence observations with the Atmospheric Imaging Assembly (AIA; Lemen et al. 2012) have revealed new information about prominence barbs and the prominence-corona transition region (PCTR; Parenti et al. 2012; Ruan et al. 2018). The Interface Region Imaging Spectrograph (IRIS; De Pontieu et al. 2014) allows for the acquisition of spectroscopic observations of prominences in the near ultraviolet (NUV) and far ultraviolet (FUV). Many past studies have focused on the information one is able to ascertain from statistics of the line profiles (Heinzel et al. 2014; Ruan et al. 2018; Kucera et al. 2018; Levens et al. 2016; Liu et al. 2015).

Recent studies have focused on attempts to invert solar prominence atmospheres to obtain diagnostic information pertaining to that of the atmospheric conditions from IRIS observations of Mg II (Jejić et al. 2018; Zhang et al. 2019; Levens & Labrosse 2019). Such inversions have been done by generating grids of models and matching them with observational data through different statistical methods. These comparisons between observed and computed spectra are based on integrated line intensities and line widths. However, these studies did not provide detailed information on how closely the models match the observations: a ‘best match’ model is always returned, even if the observed and computed line shapes are very different. Heinzel et al. (2015) fitted a computed line profile to the mean of six line profiles with a focus on the shape of the line

\(^*\) Movies associated to Figs. 10 and A.1 are available at https://www.aanda.org
profiles rather than the integrated line intensities and line widths. In this paper, a similar type of inversion is done, but here we look at each line profile separately, point-for-point, using a statistical test to assess where the models yield good comparisons with the observations.

The paper is organised as follows. In Sect. 2 we present observations of a solar prominence obtained on 19 April 2018. In Sect. 3, we perform a detailed analysis of the characteristics of the Mg II h&k line profiles observed with IRIS. In Sect. 4, we present the models used in this work and the method developed to compare models and observations, as well as the results that we obtain. In Sect. 5 we offer our conclusions.

2. Observations

A filament appeared on the south-western solar disc on 17 April 2018 in Hα observations from the Meudon Spectroheliograph1 (see Fig. 1).

This then later manifested as a prominence off the south-western solar limb on 19 April 2018. The prominence was observed with IRIS, and Hinode (Kosugi et al. 2007) as part of a coordinated observation with the Multichannel Subtractive Double Pass (MSDP) spectrograph (Mein 1991) in the Meudon Solar Tower and other ground-based observatories. The IRIS and Hinode observations start from 14:14 and end at 19:15 UTC. The IRIS observations are comprised of a set of 18 very large coarse 32-step rasters of the C ii (1331.7 Å–1358.3 Å), Si iv (1388.0 Å–1406.7 Å), and Mg ii (2783.2 Å–2835 Å) filters, along with their complimentary slit-jaw imager (SJI) observations centred at 1330 Å, 1400 Å, and 2796 Å, respectively. The rasters had a field of view (FOV) of 63.9″ × 182.3″ centred on helioprojective coordinates 632.5″, −753.2″, with a clockwise satellite rotation angle of 51°, such that the solar limb was parallel to the y axis of the instruments. The Hinode observations consisted of X-Ray Telescope (XRT; Golub et al. 2007) observations with three filter combinations, Al poly/Open, Open/Gband, and Open/Ti with an FOV of 263.3″ × 263.3″, centred on helioprojective coordinates 607.2″, −749.7″. The MSDP observations start at 12:05 UTC and end at 16:35 UTC with a reconstructed FOV of 270″ × 370″ (see Barczynski et al. 2021). AIA whole-disc observations were also available. Figure 2 shows a depiction of the configuration of the AIA, IRIS, and Hinode observations.

2.1. Hinode/XRT

The images from the Al poly/Open filter of XRT on board Hinode clearly show the coronal cavity in which the prominence sits. However, over the course of the observation, these images do not show any appreciable change or brightenings (see Fig. 3).

2.2. IRIS

The IRIS FITS files were retrieved from the Lockheed Martin Solar and Astrophysics Laboratory (LMSAL) website as level 2 FITS. Radiometric calibration was performed in Python.

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1 http://bass2000.obspm.fr
through the method described in Pereira et al. (2018), with the response function retrieved through iris_get_response.pro from SolarSoft (SSW). The data were also deconvolved through Python using a procedure following similar operations to iris_sg_deconvolve.pro from SSW. Coronal and noisy pixels were removed from the Mg\textsc{ii} rasters. This was done by calculating a histogram of the full width at half maximum (FWHM) of both Mg\textsc{ii}  h and Mg\textsc{ii}  k in every pixel of every raster. The FWHM was calculated via the quantile method (see Sect. 3). These FWHM histograms exhibit a local minimum near the centre of the distributions. Any pixel that exhibits a spectrum with a FWHM above this local minimum is assumed to be a noisy and/or coronal pixel. This can be assumed as random noise will appear to yield a large FWHM via the quantile method. However, some pixels contain spectra with more than one peak, leading to the appearance of more than one, or complex, look. This implies that some regions of the prominence have double peaked and complex line profiles. Figure 7 shows the distribution of the spectral line shapes observed by IRIS. While the distribution of line profile types is dominated by single peaked profiles, the number of double peaked and complex profiles is not negligible – with approximately 20\% of line profiles appearing complex.

In this paper, we focus on the Mg\textsc{ii} (NUV) filter. The prominence only appears very faintly in the Si\textsc{iv} and C\textsc{ii} rasters, making analysis of the FUV bands difficult. We note that reducing the colour-bar limit of the FUV SJI images enough to see the prominence at this low intensity leads to the manifestation of a ghost image of the aperture of the telescope. This is due to parasitic infrared and visible light and only affects off-limb observations in the FUV channels; the NUV channel is unaffected (Wülser et al. 2018).

In the 2796 Å SJI images, the prominence shows very dynamic behaviour with many flows towards the south-western limb. This culminates in a large flow extending down from a rise of material seen to branch out from the main section of the prominence that persists through the observation. These three stages are shown Fig. 5.

2.3. AIA

The AIA files were retrieved from the Virtual Solar Observatory (VSO) as level 1 FITS. These were then prepared to level 1.5 through the use of aia_prep.pro from SSW in IDL. The 304 Å filter shows a similar evolution to that seen in the Mg\textsc{ii} k SJI from IRIS. This is expected as the emission in both channels have some chromospheric origins (De Pontieu et al. 2014; Lemen et al. 2012). The limb, however, appears higher in 304 Å than in Mg\textsc{ii} k; this is likely due to the transition region contribution to the 304 Å filter.

The 171 Å filter clearly shows a small pillar-like barb extending into the region where the prominence is clearly seen in chromospheric filters. This corresponds to the central and densest part of the prominence. One would expect to see strong central reversals in the Mg\textsc{ii} h\&k spectra (see Sect. 3) in this area owing to the high density of material. This is where the prominence appears to be anchored to the surface. In 171 Å, we also observe a fainter structure enveloping the barb. This can be interpreted as the PCTR since the region of the solar atmosphere imaged by 171 Å includes the upper transition region (TR).

After the end of the IRIS and Hinode observations, the prominence is still seen in the 171 Å and 304 Å filters of AIA. In 304 Å the prominence remains fairly dynamic and appears to fall away towards the limb over the next 24 hr. This can be attributed to the projection effect and the prominence is simply rotating out of view. A similar conclusion is drawn from the 171 Å filter. However, the PCTR and barb of the prominence appear to fade over the next 24 hr as emission from brighter coronal material begins to occult these structures. No filament eruption is observed. On 22 April, the structure reappears in the 171 Å and 304 Å EUVI filters of the Sun Earth Connection Coronal and Heliospheric Investigation (SECCHI; Howard et al. 2008) on board the Solar Terrestrial Relations Observatory (Ahead) (STEREO-A; Driesman et al. 2008) and continues to transit across the disc. At this time, the angular separation of STEREO-A from the Earth was approximately 117°.

3. IRIS spectra

Some of the Mg\textsc{ii} h\&k spectra obtained by IRIS show complex structure. This implies that some regions of the prominence have more than one structure along the line of sight. A notable example is seen in the top of Fig. 6 near 120° in slit position 7. Here we see what appears to be a single peaked profile in Mg\textsc{ii} h\&k with a secondary redshifted peak. This is not unique to this slit position, though this is the most extreme case. There are many areas where line profiles are composed of many intensity peaks. These lead to the appearance of more than one, or complex, looking line profiles. Figure 7 shows the distribution of the spectral line shapes observed by IRIS. While the distribution of line profile types is dominated by single peaked profiles, the number of double peaked and complex profiles are not negligible – with approximately 20\% of line profiles appearing complex.

Here we use the quantile method (Kerr et al. 2015; Ruan et al. 2018) to determine the FWHM, line core shift, and asymmetry of the line profiles to investigate the internal structure and dynamics of the prominence. The quantile method involves calculating the cumulative distribution function (CDF) of the
Fig. 5. Three main stages of the evolution of the prominence. The top, middle, and bottom rows show, Mg ii IRIS/SJI, 304 Å SDO/AIA, and 171 Å SDO/AIA, respectively. The left, centre, and right columns show small flows from main body, the end of the rise of material, and the large flow of this risen material, respectively.

intensity of the individual line profiles over some wavelength range. Here, we employ a 3 Å window centred on the rest vacuum wavelengths of Mg ii h&k. The wavelength at which the 50% level of the CDF is found (λ_{50}) is defined as the line core. The FWHM can be calculated by taking the difference between the wavelength at which the 88% (λ_{88}) and the 12% (λ_{12}) level of the CDF is found. Additionally, the asymmetry of the line profiles is calculated by,

\[
\text{Asymmetry} = \frac{λ_{88} - λ_{50}}{λ_{88} - λ_{12}}.
\]

The rest wavelengths of the Mg ii h&k line cores were calculated by performing quantile analysis on every pixel of the first slit position of every raster, taking λ_{50} as the line core. This was done as the first slit position of each raster is on the solar disc, which gives us a rotation independent measure of the line cores. We use the nominal wavelength calibration provided in the data header. From this, 9360 measurements of the line core were obtained for h&k, of which the mean was taken. The rest wavelengths for the Mg ii h&k line cores were found to be 2803.494 Å and 2796.348 Å respectively, whereas the rest vacuum wavelengths are 2803.53 Å and 2796.35 Å respectively (Levens & Labrosse 2019). The spectral resolution of the Mg ii observations were 0.051 Å, giving these measured values an error of ±0.0255 Å.

The calculated wavelengths of the line cores are used here as reference wavelengths in order to effectively transform into the inertial frame of the solar limb such that its rotation is not included in the line core shift calculations.

3.1. Line profile distribution

The prominence presents a variety of line profile types. These were found by using a finite difference approximation of the derivative of values above the standard deviation of the intensity of the currently considered pixel. From this, stationary points could be counted. If two, or more than three stationary points were found, the line profile was classified as complex. Such a complex line profile is discussed in Sect. 3.3. Figure 7 shows
an example of the distribution of line profile types in raster 15. Parts of the prominence nearest the edges of the structure are more likely to exhibit single peaked behaviour relative to those in nearer the centre. Those under motion also favour single peaked behaviour.

We observe a large arm extending from the main body of the prominence near the end of the observation that displays mainly single peaked line profiles. This arm also contains a few classic double peaked line profiles. In addition, it exhibits complex profiles that appear to be double peaks suffering from the effect further discussed in Sect. 3.2 where the emission of $h_3$ and $k_3$ is greatly reduced, resulting in only $h_2$ and $k_2$ peaks. This is due to the intensity of $h_2$ and $k_2$, peaking lower than $h_3$ and $k_3$, which causes no defined peaks at these locations. Double peaks in the
arm can be interpreted in one of two ways – there is a large volume of material in the arm along the line of sight or there exists more than one strand in the composition of this arm with different line-of-sight velocity shifts. In the former case, the optical thickness of the plasma would result in a double peaked profile. However, judging by the extent of the arm in the plane-of-sky, this interpretation is unlikely. For it to be extended enough along the line of sight to cause this effect, it would mean it would take the form of a sheet-like structure and we see no evidence of this morphology. A more plausible interpretation is the latter. This would lead to a measured line core shift, as if it were the former case, resulting in a lower measured velocity. This may also be another reason for the broadened wings of the line core shift distribution discussed in Sect. 3.2. Admittedly, this would be a rather small effect on the distribution,! and the more likely cause is the effect that asymmetry has on measured Doppler velocity due to the increased emission of the red or blue sides of these line profiles. This effect is discussed in detail in Sect. 3.2.

The double peaked line profiles of the main body of the prominence are most likely due to a large amount of material along the line of sight. The optical thickness would assist in producing the classic double peaked look of Mg II h&k emission. The pixels classified as complex in Fig. 7 are likely due to many different structures or threads in that pixel. These areas of complexity appear to correlate with areas of large FWHM and asymmetry, giving more evidence towards this interpretation. The south-eastern edge of the prominence displays mainly asymmetry, giving more evidence towards this interpretation. The pixels classified as complex in Fig. 7 are likely due to this effect. It is therefore sensible to assume these

3.2. Line core shift

We calculate line core shifts by computing the Doppler velocity of each pixel using the 50% quantile ($\lambda_{50}$) of each pixel as the line core. From this, we find a range of line core shifts in the prominence, with the extrema ranging from −74 to 78 km s$^{-1}$ in Mg II h and −72 to 85 km s$^{-1}$ in Mg II k. The total distribution is Gaussian-like centred on a redshifted line core of around 8.20 km s$^{-1}$ and 5.20 km s$^{-1}$ with standard deviations of 5.98 km s$^{-1}$ and 6.61 km s$^{-1}$ in Mg II h&k, respectively. These distributions can be seen in Fig. 8.

Mg II h&k line shifts are an excellent diagnostic tool for the Doppler velocities seen in the structure (Leenaarts et al. 2013). These recovered velocities are quite typical of past prominence observations. Liggett & Zirin (1984) observed velocities ranging from 12 to 75 km s$^{-1}$, and Schmieder et al. (2017) found maximum velocities of around 60 km s$^{-1}$ . Table 6 in the review by Labrosse et al. (2010) shows a range of velocities exhibited by prominences in the EUV, with an extremum of 70 km s$^{-1}$, centred around 20 km s$^{-1}$.

The wings of the Gaussian fits used in Fig. 8 do not seem to model the velocity distributions well. The cause of this shape is suggested by Fig. 9. Asymmetry and measured Doppler velocity appear to be anti-correlated, plateauing at high measured velocities. The root of this trend lies in the optical thickness of the lines. At rest, the line cores of Mg II h&k are optically thick, but the wings are optically thin. Therefore, line profiles of high redshift will display a negative (red) asymmetry due to h&k and k$^v$ being shifted into the more optically thick area of the line. This leads to the quantile method measuring a larger-than-true velocity due to the absorbed h&k and k$^v$, giving more credence to the intensity of h&k and k$^v$. This effect is amplified by h&k and k$^v$ moving more into the optically thin regime of the wings. The opposite is also true for the blueshifted profiles that see absorption and enhancement of h&k, and h&k, and h&k, respectively. The extensions of the wings of the Doppler velocities are likely due to this effect. It is therefore sensible to assume these
high velocities are measured to be larger than in reality, and the true distribution may still be of a Gaussian shape. The velocities of areas where the asymmetry is much greater than zero are likely unreliable, and only those where the asymmetry is approximately 0, can be considered reliable.

3.3. Line widths

Here, we use the difference between the 88% and 12% quantiles \((\lambda_{88} - \lambda_{12})\) to measure the FWHM, as in Ruan et al. (2018). If you assume that the line profiles are of a Gaussian shape, the difference between the 88% and 12% quantiles is the FWHM. FWHM maps clearly separate the prominence (and spicules) from the solar disc. They also separate the prominence and solar disc from the background corona as discussed in Sect. 2.2. These FWHM maps allow for the location of flows and structures not easily seen in intensity maps. The FWHM of the lines profiles within the prominence are relatively small, ranging from around 0.1 Å to 0.6 Å, whereas the FWHM within the solar disc have values of around 0.8 Å–1 Å. In the first raster (14:13UTC; see Fig. 10), we see a structure of large FWHM, in comparison to the same location in later rasters, around (10") 110") This structure is seen in both Mg II h&k, suggesting that this is a physical phenomena. On further inspection, the spectra in both Mg II h&k, in this area, show two distinct line profiles, one of which is highly redshifted. The shape and location of this structure seems very similar to that of the pillar-like barb easily seen in 171 Å. One of the drawbacks of the quantile method here is that it cannot distinguish between line profiles. If a pixel displays more than one line profile, or one of a more complex nature, the algorithm is still able to produce a number for this, albeit a large one. This can then be used as a proxy for whether a spatial pixel contains more than one line profile.

3.4. Asymmetry

Asymmetry is most apparent in the extended arm protruding from the main prominence body as seen in raster 15 (see Fig. 10). Most emission in this area is seen to have asymmetry in the range \([0, -1]\). However, these line profiles may just have too low of an intensity, which gives too much credence to the noise in the quantile analysis. Many of these profiles do not appear asymmetric, just highly Doppler shifted. This can be seen in Fig. 10 as the areas of high redshift appear to correlate to those of non-negligible asymmetry and low integrated intensity. However, there does appear to be an anticorrelation between the line core shift and the asymmetry as can be seen in Fig. 9. The only structure that appears to break this trend, is the structure of large FWHM discussed in Sect. 3.3. Its large asymmetry is likely due to the two line profiles seen in this area, leading to a erroneous measurement of asymmetry. This shows that asymmetry calculated via the quantile method, when combined with its complimentary FWHM, is a better proxy for whether a pixel contains more than one line profile than either diagnostic on its own.

4. Model comparisons

Levens & Labrosse (2019) discussed an extension to the one-dimensional radiative transfer code developed by Gouttebroze et al. (1993), PROM, such that it was able to produce Mg II line profiles with both isobaric and isothermal atmospheres, and atmospheres containing a PCTR. The latter atmosphere was itself added as an extension by Labrosse & Gouttebroze (2004). This Mg II is independently developed. In this model, prominences are represented by a one-dimensional semi-infinite plane-parallel slab perpendicular to the solar surface. This block is illuminated by the solar disc. They also separate the prominence and solar disc from the background corona as discussed in Sect. 2.2. These FWHM maps allow for the location of flows and structures not easily seen in intensity maps. The FWHM of the lines profiles within the prominence are relatively small, ranging from around 0.1 Å to 0.6 Å, whereas the FWHM within the solar disc have values of around 0.8 Å–1 Å. In the first raster (14:13UTC; see Fig. 10), we see a structure of large FWHM, in comparison to the same location in later rasters, around (10") 110") This structure is seen in both Mg II h&k, suggesting that this is a physical phenomena. On further inspection, the spectra in both Mg II h&k, in this area, show two distinct line profiles, one of which is highly redshifted. The shape and location of this structure seems very similar to that of the pillar-like barb easily seen in 171 Å. One of the drawbacks of the quantile method here is that it cannot distinguish between line profiles. If a pixel displays more than one line profile, or one of a more complex nature, the algorithm is still able to produce a number for this, albeit a large one. This can then be used as a proxy for whether a spatial pixel contains more than one line profile.

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model reaches the end of the spectral window. The lowest measured RMS from this ‘roll’ is recorded, along with the pixel shift required to achieve this. The next model in the set is then tested. This process is repeated until all of the models have been tested. This is run for both h&k. The RMS values for h&k are then summed, and the model that produces the lowest overall RMS sum is then selected as the model indicative of the plasma parameters if the RMS is lower than a certain threshold. RMS values that are larger than that threshold indicate that the computed and observed line profiles are too different, and that no model could be found to satisfactorily reproduce the observed line profiles.

By ‘rolling’ our models through the spectral window, this gives us a measure of the wavelength of the line core (from the recorded pixel shift required to minimise the RMS) and allows us to calculate a Doppler velocity. The rolling RMS (rRMS) procedure is also able to measure pixel shift with sub-pixel precision. However, the run time of the procedure scales linearly with the number of sub-pixels requested. This works identically to without sub-pixel precision, but before the rolling begins, the...
models and data are interpolated up to match the sub-pixel precision requested.

4.1. Results

After the procedure was run, twelve line profiles were selected at random to illustrate where the procedure found good matches and where it did not (see Fig. 11).

The goodness of these fits were judged by eye. The measured RMS of these twelve line profiles were used to arrive at a cut off value above which matches would be considered unsatisfactory. This value was determined to be 15 000, concluding that 49%, 35 617 \( \times \) 10, of the matches were satisfactory. Figure 12 shows that areas of higher k/h ratio weakly correlate with areas that give a satisfactory fit. High values of the k/h ratio are related to areas of lower optical thickness. Therefore, this demonstrates that areas of lower optical thickness lead to better matches with the models. This could also be due to the one-dimensional nature of the code as the satisfactory fits seem to also correlate with areas of single peaked line profiles, as seen in Fig. 7. These values for the k/h ratio appear to be consistent with Alissandrakis et al. (2018) where they found a k/h ratio of 1.22 on approach to the limb and values up to 1.96 in the spicules.

Figure 13 shows that in the most part, areas in which we see \( \text{H} \alpha \) emission in the prominence correspond to where computed \( \text{Mg} \) line profiles do not satisfactorily match the observed ones. The observed \( \text{H} \alpha \) line profiles are generally complex in shape and much wider than the models produce. This issue is seen when attempting direct one-dimensional forward modelling of \( \text{H} \alpha \) prominences. For example, Ruan et al. (2019) demonstrated that areas with wide \( \text{H} \alpha \) line profiles can be better fit by models with high microturbulent velocities. Whether this is also true for \( \text{Mg} \) line profiles is currently unclear. Figure 14 presents the temporal evolution of the mean pressure and mean temperature as derived from the comparison between computed and observed \( \text{Mg} \) line profiles, while Fig. 15 shows these parameters for the pixels in rasters 1, 12, and 15 recovered by the procedure. Figure 16 presents diagnostic maps for electron density, ionisation degree, \( \gamma \) (i.e. temperature gradient), and column mass for raster 15. We stress that the plasma parameters obtained with this method are only reliable where our RMS values are low enough, as indicated with the satisfactory matches in the right panel of Fig. 12.

4.1.1. Pressure

The mean pressure appears to remain stable during the IRIS observation, with the mean pressure fluctuating on average between 0.18 and 0.26 dyne cm\(^{-2}\) (Fig. 14). The pressures of 1 dyne cm\(^{-2}\) found towards the core of the structure correlate closely with the unsatisfactory fits (Fig. 15). This high pressure is at the upper limit of that outlined in Table 1 of Labrosse et al. (2010). These selected models could be explained by the procedure finding that broadened profiles produce a smaller RMS for line profiles that exhibit a complicated structure due to the large volume of the prominence to travel through (a larger optical depth) coupled with many different threads along the line of sight as seen in this area of the prominence. Pressure near the outer edges of the prominence is, in general, lower as we move through the PCTR towards the corona where the gas pressure is lower (Aschwanden 2004).

4.1.2. Temperature

The mean temperature, like pressure, also appears stable during the observation, with the mean temperature staying on average between 7800 K and 11 500 K (see Fig. 14). This is consistent with expected results. The formation height of \( \text{Mg} \) ranges from the upper photosphere to the upper chromosphere (De Pontieu et al. 2014). However, in a prominence, we expect a range of chromospheric to PCTR temperatures. The temperature of the prominence increases towards the outer edges where one would expect to see the PCTR in the plane of sky (Fig. 15). Figure 16 further reveals higher values nearer to the edges of the prominence. The arm seen near the end of the observation appears to be a tenuous and hot structure reaching upper chromospheric temperatures of a few 10\(^3\) K.

Equation (2) describes the relationship between \( \gamma \) and the temperature profile \( T(m) \) (a function of column mass). In Table 1, models where \( \gamma = 0 \) in fact correspond to isothermal and isobaric models without a PCTR. Many of the satisfactory fits having \( \gamma \neq 0 \) shows that the PCTR extension to PROM by Labrosse & Gouttebroze (2004) implemented into the \( \text{Mg} \) extension by Levens & Labrosse (2019) is important to obtain a better agreement to the data than isothermal and isobaric models. Our mean temperatures are greater than temperatures obtained by Zhang et al. (2019). However, the authors of that study employed isobaric and isothermal models whereas our models include a PCTR, as mentioned before. This allows our inferred mean temperatures to be much greater. Areas where \( \gamma = 0 \), indicating isothermal models, correlate with areas of lower temperature, which agrees with their study. In future, a finer grid of \( \gamma \) values could help with a better resolution of the temperature gradient of the PCTR.

4.1.3. Column mass

The mass along the line of sight conveys that the extensions of the prominence have comparatively low mass (Fig. 16). The region where unsatisfactory fits are found is much higher density than the surrounding material. While these fits may be unsatisfactory, we can infer from the line profiles of that area that there are several threads along the line of sight that contribute to the line profiles. This includes profiles such as those shown in Fig. 17. The unsatisfactory fits here are due to the single slab nature of the models, which does not account for several threads along the line of sight. A single slab model can only apply, when there are several threads, if the threads are comoving, which would result in a single line profile. The arm seen near the end of the IRIS observations appears to be comparatively low mass. This explains the single peaked line profiles observed in the arm. The intensity of the central reversal is anticorrelated with

| Parameter | Unit | Value |
|-----------|------|-------|
| \( T_{\text{cen}} \) | K | 6000, 8000, 10 000, 15 000, 20 000, 25 000, 30 000, 35 000, 40 000 |
| \( T_H \) | K | 100 000 |
| \( P_{\text{cen}} \) | dyne cm\(^{-2}\) | 0.01, 0.02, 0.05, 0.1, 0.2, 0.5, 1 |
| \( P_\gamma \) | dyne cm\(^{-2}\) | 0.01 |
| Slab width | km | 200–124 100 |
| \( M \) | g cm\(^{-2}\) | 3.7 \( \times \) 10\(^{-5}\)–5.1 \( \times \) 10\(^{-4}\) |
| \( v_T \) | km s\(^{-1}\) | 5 |
| \( H \) | km | 1000 |
| \( \gamma \) | | 0, 2, 5, 10 |
Fig. 11. Four of the twelve random line profiles where a good fit is found for six and an unsatisfactory fit is found for the other six. The top two panels are the unsatisfactory fits, and the bottom two panels are the satisfactory fits.

Fig. 12. Comparison of \( k/h \) ratio and satisfactory fits. This demonstrates the weak correlation between high \( k/h \) ratio and satisfactory fits. Left: \( k/h \) ratio of raster 15. Right: satisfactory fits of raster 15. Raster 15 was taken between 18:08 and 18:25 UTC.

formation height due to optical depth (Leenaarts et al. 2013). This reinforces the finding of low column mass not just in the arm, but where single peaked line profiles are observed.

4.1.4. Electron density

The majority of the prominence appears to have an electron density of less than \( 0.6 \times 10^{11} \) cm\(^{-3} \), with the exception of a few places where it is greater than \( 1 \times 10^{11} \) cm\(^{-3} \) (Fig. 16). The arm appears to be of generally comparatively low electron density. Even though it is of a comparatively high temperature compared to the rest of the prominence, its low pressure can explain the low electron density found.

4.1.5. Ionisation degree

Ionisation degree is defined by the mean number density of H\( \text{II} \) \( (n_{\text{HII}}) \) to H\( \text{I} \) \( (n_{\text{HI}}) \) (Tandberg-Hanssen 1995). Past works (such as Zhang et al. 2019) assume that the mean number of electrons \( (n_e) \) is equal to the mean number of protons \( (n_p) \), and further that the mean number of protons is equal to the mean number density of H\( \text{II} \) and that the mean number density of H\( \text{I} \) is dominated by the mean number density of ground state Hydrogen \( (n_{\text{H0}}) \) then,

\[
\frac{n_{\text{HII}}}{n_{\text{HI}}} \approx \frac{n_e}{n_{\text{H0}}}.
\] (4)

However, the assumption that \( n_e \approx n_p \approx n_{\text{HII}} \) does not hold with PROM because not all of the electrons are liberated from H\( \text{I} \). There is a fixed contribution of electrons from other species, such as helium, that contribute to the total number of electrons (named excess electrons from here on). This increase is most apparent at high temperatures when the number density of H\( \text{II} \) and excess electrons increase dramatically. Figure 18 shows the behaviour of ionisation degree and excess electrons with increasing temperature. At temperatures above 30,000 K, these species are responsible for a 20\% increase in the total number of electrons (see Fig. 18 bottom). So here we focus on the definition from Tandberg-Hanssen (1995). Some sections of the prominence are found to have a very large ionisation degree when compared to past studies. Vial (1998) summarised that the
ionisation degree in a prominence does not change much with temperature, given that the density is low. This was based on studies by Gouttebroze et al. (1993) and Heinzel et al. (1994). However, the highest temperature considered in these studies is 15,000 K. Figure 18 shows that the ionisation degree is fairly constant up until 15,000 K, consistent with these studies, but then rises sharply at higher temperatures. Additionally, at 15,000 K, the excess electrons are responsible for only a roughly 7% increase in the number of free electrons (as in Fig. 18 bottom).

The areas where a high ionisation degree is found (see top right panel of Fig. 16) correlate strongly with areas of high mean temperature and non-zero values of gamma. The model that yields the highest ionisation degree has a central temperature of 40,000 K and a surface temperature of $10^5$ K.

### 4.2. Recovered line core shift

Due to the rolling aspect of the procedure, we recover a measure of the line core shift. The resolution of the line core shifts from the rolling RMS procedure is 2.7 km s$^{-1}$. This comes from the minimum measurable line core shift that is equal to the wavelength resolution of the instrument, divided by the number of sub-pixels plus 1. Figure 19 shows the line core shift measured by the quantile method and measured by the rolling RMS procedure. These plots qualitatively agree. With the other diagnostics, there is a degree of scepticism surrounding regions where unsatisfactory fits were found. However, while those models do not represent the underlying conditions of the prominence in those regions, the fit found by the procedure will still give a good measure of line core shift. The lowest RMS will be found where the model profile is centred on the data profile, regardless of how good the fit is. Therefore, we can reasonably trust the line core shifts found by the rolling RMS procedure, even in regions where unsatisfactory fits are found.

Figure 20 shows a similar plot to that of Fig. 8, but for the line core shift recovered by the rolling RMS procedure. Fewer bins are used in the histogram of Fig. 20 than in Fig. 8 as the velocity resolution of Fig. 8 is much greater than that of Fig. 20. The distributions in Fig. 20 display a Gaussian-like distribution, similar to what is found in Fig. 8, centred on a redshifted line core of around 5.3 km s$^{-1}$ and 5.6 km s$^{-1}$ with standard deviations of 9.8 km s$^{-1}$ and 10.2 km s$^{-1}$ in Mg II h&k respectively. Due to the limited resolution of the line core shifts recovered by the rolling RMS procedure, an estimate of the uncertainty on these values is given as $\pm 1.35$ km s$^{-1}$, half of the velocity resolution of the recovered line core shift. The central line core shift.
shift of Mg II k found by the quantile method, is within the uncertainty of the central line core of Mg II k recovered by the rolling RMS procedure. However, the central line core shift of Mg II h does not give the same result. This could be due to the introduced asymmetry bias discussed in Sect. 3.2.

5. Conclusions

The prominence observed on the south-western solar disc on 19 April 2018 exhibited many dynamic flows seen both in AIA and IRIS. These flows were best seen in chromospheric filters. Coronal filters showed the barb of the prominence, and when it was
sufficiently raised in altitude, an outline of the PCTR was also seen. From the line core shift measurements via the quantile method, we find that the prominence is dominated by redshifted flows relative to the solar disc. Large values of asymmetry can be attributed to the plasma moving fast enough such that part of the line is emitted in the optically thin regime, closer to the wings of Mg II h&k emission from plasma at rest. This resulting large asymmetry biases the line core shift calculations to be redder or bluer depending on the direction that the plasma is moving and as such measures higher magnitudes for line core shift than would be expected if it were emitted closer to the rest line core. Therefore, using this method, the distribution of line core shifts may deviate from the expected Gaussian shape in the wings of the line core shift distribution. The prominence exhibited a wide range of line profile shapes, a majority of which were single peaked, due to the low column mass exhibited by the majority of the prominence.

Through comparisons with one-dimensional radiative transfer models, we retrieve internal plasma diagnostics of the prominence. The prominence was found to display a wide range of pressures, ranging from 0.01–0.5 dyne cm$^{-2}$. Mean temperatures ranged from 6000–50 000K. These results included models with a PCTR, so while these temperatures may seem higher than classically thought of in a prominence, these suggest the line of sight intercepts the prominence material and much of the PCTR. We also note that the high mean temperature values returned by the models fitting the Mg II lines are found in areas where there is no detectable Hα emission. This demonstrates the importance of the inclusion of the PCTR in prominence modelling. The column mass ranges from $3.7 \times 10^{18}$–$5 \times 10^{19}$ g cm$^{-2}$.

The line core shifts recovered from our Mg II line profile comparison procedure agree well with the measured line core shifts for Mg II k. For Mg II h, they are of the same order of magnitude. This demonstrates that the unsatisfactory fits are not a result of the rolling RMS procedure but are a consequence of the limitations of the one-dimensional radiative transfer models. Models with multiple threads (Labrosse & Rodger 2016; Gunär et al. 2007, 2008) are likely to produce line profiles in better agreement with the observations.

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4.0.1 of Astropy, (http://www.astropy.org) a community-developed core Python package for Astronomy (Astropy Collaboration 2013, 2018)

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Appendix A: Mg\textsc{ii} k diagnostic maps

![Mg\textsc{ii} k statistics maps](image)

Fig. A.1. Mg\textsc{ii} k statistics maps of the three main stages of the prominence observation calculated via the quantile method. The times associated with these plots are the time at the beginning of the associated raster. The dashed lines represent the slit positions in Fig. 6. An animated version of this figure is available online.