A measurement of galaxy halo mass from the surrounding H I Ly\(\alpha\) absorption

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ABSTRACT
We measure the dark matter halo masses of \(z \approx 2.36\) UV color-selected star-forming galaxies by matching the observed median H I Ly\(\alpha\) absorption around them, as observed in the spectra of background QSOs, to the absorption around haloes above a given mass in cosmological simulations. Focusing on transverse separations 0-2 pMpc and line of sight separations 154-616 \(\text{km s}^{-1}\), we find a minimum halo mass of \(\log_{10} M_{\text{min}}/M_\odot = 11.6 \pm 0.2\), which is in good agreement with published halo mass estimates from clustering analyses. We verified that the measured halo mass is insensitive to a change in the cosmological parameters (WMAP1 vs. WMAP3) and to the inclusion of strong AGN feedback. One unique strength of this method is that it can be used in narrow field galaxy-QSO surveys, i.e. \(\approx 30 \times 30\) arcseconds. In addition, we find that the observed anisotropy in the 2-D H I Ly\(\alpha\) absorption distribution on scales of 1.5-2 pMpc is consistent with being a consequence of large-scale gas infall into the potential wells occupied by galaxies.

Key words: galaxies: high-redshift — intergalactic medium — quasars: absorption lines

1 INTRODUCTION
The mass of the host dark matter halo is believed to be a key factor determining galaxy evolution. Measuring halo masses is therefore an important goal of observational astronomy. For clusters of galaxies, the employed techniques include measurements of the Sunyaev-Zeldovich effect (e.g. Sunyaev & Zeldovich 1972; Motl et al. 2005), cluster X-ray temperature and luminosity (e.g. Reiprich & Böhringer 2002), strong lensing (e.g. Gavazzi et al. 2007), weak lensing (also called galaxy-galaxy lensing; e.g. Kaiser & Squires 1993), and kinematics of galaxies (e.g. Zwicky 1937). Measuring dark matter halo masses of individual galaxies is more difficult and usually requires statistical methods such as stacking combined with weak lensing (e.g. Mandelbaum et al. 2006), satellite kinematics (e.g. More et al. 2011), clustering analysis (e.g. Kaiser 1984), or abundance matching (e.g. Conroy et al. 2006). Note, however, that Haas et al. (2011) found that the most popular environmental indicators (e.g. the number of galaxies within a given distance, or the distance to the Nth nearest neighbour) correlate strongly with halo mass and can thus be used to estimate halo masses of single galaxies.

While weak lensing has been successful in estimating dark matter halo masses for low-redshift galaxies, it is not a viable method for high-redshift objects since the lensing cross-section peaks half way towards the background galaxy, and is thus very small at \(z \gtrsim 2\). Furthermore, the number of both foreground and background galaxies becomes too low to obtain statistical samples, and measuring shapes of galaxies becomes increasingly hard.

As known from structure formation studies, more massive dark matter haloes cluster more strongly than lower mass haloes, and on scales greater than the haloes, the galaxies inhabiting such haloes cluster similarly as their host haloes. Matching the observed clustering properties of a given galaxy population with the clustering of haloes in N-body simulations leads to estimates of the most likely host halo masses. This method has facilitated some important insights into the properties of galaxies, and their likely descendants (e.g. Adelberger et al. 1998, 2005b; Quadri et al. 2007; Conroy et al. 2008).

Here we measure galaxy halo masses from H I Ly\(\alpha\) absorption profiles. Numerous studies have shown that the mean absorption of the light from a background object (e.g. a bright QSO) is increased

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when the sightline passes near a foreground galaxy, both observationally (e.g. Chen et al. 1998, 2001; Penton et al. 2002; Adelberger et al. 2003, 2005; Croft et al. 2005; Prochaska et al. 2011; Rakic et al. 2011, 2012; Rudie et al. 2012), and using simulations (e.g. Croft et al. 2002; Kollmeier et al. 2003; Bruscoli et al. 2003; Desjacques et al. 2004; Kollmeier et al. 2006; Desjacques et al. 2006; Tasker & Bryan 2006; Bertone & White 2006; Stinson et al. 2012; Ford et al. 2012). At high-redshift this enhancement can be calculated statistically out to distances of several proper Mpc (pMpc). Kim & Croft (2008) proposed to use such absorption profiles to measure halo masses of foreground QSOs and galaxies. Somewhat related to this method is the work of Faucher-Giguère et al. (2008), who presented the 2-D (i.e. along the line of sight, LOS, and in the transverse direction) absorption distribution around UV selected star-forming galaxies from the Keck Baryonic Structure Survey, KBSS (Steidel et al., in preparation), at \( z \approx 2.36 \). Through the analysis of the absorption spectra of background QSOs they found enhanced Ly\( \alpha \) absorption within \( \approx 3 \) proper Mpc (pMpc) from galaxies. They also presented the 2-D (i.e. along the line of sight, LOS, and in the transverse direction) absorption distribution and they measured a slight compression of the signal along the LOS on scales \( \gtrsim 1.5 \) pMpc. This compression suggests large-scale infall of gas into the potential wells occupied by the galaxies. 

This observational study is particularly suitable for testing the method because the dark matter halo masses of the galaxies are already known from clustering analyses (e.g. Adelberger et al. 2005b; Conroy et al. 2008; Trainor & Steidel 2012; Conroy et al. 2008) found that every halo at \( z \sim 2 \) with \( M_h > 10^{11.5} h^{-1} M_\odot \) hosts a star-forming galaxy from the photometric sample from which the galaxies used in R12 were drawn. This result was obtained using N-body simulations with the WMAP year-1 cosmology. Using the WMAP year-3 cosmology (which is what the simulations in this paper are based on), they found an 0.3-0.4 dex smaller minimum halo mass. Using a spectroscopic sample that is almost identical to the one used by R12, Trainor & Steidel (2012) found that these galaxies reside in halos with \( M_h > 10^{12.5} h^{-1} M_\odot \), using WMAP year-7 cosmological parameters.

The paper is organized as follows. We describe the simulations in Section 2. The method for measuring halo mass is presented in Section 3. We discuss the origin of the observed redshift space distortions seen in the 2-D absorption maps from R12 in Section 4. Finally, we conclude in Section 5. The appendix demonstrates that our results are converged with respect to the numerical resolution and the box size of our simulations.

Throughout the text proper distances are denoted as pMpc, and comoving as cm/pc.

2 SIMULATIONS

We use a subset of simulations from the suite of OverWhelmingly Large Simulations (OWLS; Schaye et al. 2010). The simulations were run using a modified version of GADGET-3 (last described in Springel 2005), which is a Lagrangian (SPH) code. These simulations include star formation (Schaye & Dalla Vecchia 2008), supernova (SN) feedback (Dalla Vecchia & Schaye 2008), radiative heating and cooling via 11 elements (hydrogen, helium, carbon, nitrogen, oxygen, neon, magnesium, silicon, sulphur, calcium, and iron) in the presence of the cosmic microwave background and the Haardt & Madau (2001) model for the ionizing background radiation from galaxies and quasars (Wiersma et al. 2009a), and chemodynamics (abundances of elements released by type Ia and type II SNe, stellar winds, and asymptotic giant branch stars; Wiersma et al. 2009b). The assumed initial mass function (IMF) is that of Chabrier (2003), with stars ranging in mass from 0.1 to 100 \( M_\odot \). Stars with masses greater than \( 6 M_\odot \) die as SNII, injecting \( \sim 10^{51} \) erg of energy into their surroundings. About 40% of this energy is injected kinetically, where particles are kicked at a velocity of 600 km s\(^{-1}\). The mass loading parameter, \( \eta \), is set to 2, i.e. the total mass of the particles that are kicked is on average equal to twice the mass of the star particle. The box sizes and (the initial) baryonic and dark matter particle masses of the simulations used here are specified in Table 1. The cosmological parameters used in the simulations are from the Wilkinson Microwave Anisotropy Probe (WMAP) year-3 results (Spergel et al. 2007), \{\Omega_m, \Omega_b, \Omega_\Lambda, \sigma_8, n_s, h\} = \{0.238, 0.0418, 0.762, 0.74, 0.951, 0.73\}.

We use the ‘reference’ (REF) model, the model with AGN feedback (AGN), the model using the ‘Millennium cosmology’ and more efficient feedback (MILL), and a model with the same SN feedback prescription as MILL but the WMAP year-3 cosmology (WML4). All of the models are described in detail by Schaye et al. (2010); here we provide only short descriptions and a brief summary can be found in Table 2.

The REF and the AGN models are identical, except that the latter includes prescriptions for the growth of supermassive black holes and for AGN feedback. These processes are implemented using modified versions of those of Springel (2005), and are described in Booth & Schaye (2009). Black holes inject 1.5 % of the rest-mass energy of accreted gas in the form of heat into the surrounding matter. Booth & Schaye (2009, 2010) show that this efficiency results in excellent agreement with the observed, \( z \approx 0 \) scaling relations between black hole masses and the properties of their host galaxies. We chose this simulation to test the effect of extreme feedback on our results as it could potentially influence the physical properties (e.g. the density and temperature) of the absorbing gas near galaxies.

To test the effect of the cosmological parameters, and to facilitate comparisons with previous studies that used older estimates of these parameters, we employ the ‘Millennium cosmology’ (Springel et al. 2005) in our MILL simulation. The MILL simulation uses the cosmological parameter values \{\Omega_m, \Omega_b, \Omega_\Lambda, \sigma_8, n_s, h\} = \{0.25, 0.045, 0.75, 0.9, 1.0, 0.73\}. As found by e.g. Conroy et al. (2008) and Trainor & Steidel (2012), the lower values of \( \sigma_8 \) that are implied by more recent WMAP results cause the lower mass dark matter haloes to cluster more strongly than in models with higher \( \sigma_8 \). Hence the minimum mass of haloes implied by the observed clustering of a galaxy population is lower. The faster growth of structure in the MILL simulation also causes higher predicted global star-formation rate (SFR) densities. The mass loading factor for the SN driven winds is therefore doubled in comparison with the REF model, to \( \eta = 4 \). This is done in order to match the peak in the observed star-formation history (SFH). We note that the WMAP year-7, estimates of cosmological parameters (Komatsu et al. 2011), \{\Omega_m, \Omega_b, \Omega_\Lambda, \sigma_8, n_s, h\} = \{0.272, 0.0455, 0.728, 0.81, 0.967, 0.704\}, prefer a value of \( \sigma_8 \) that is intermediate between those from WMAP year 1 and WMAP year 3, while the value for \( \Omega_m \) is closer to that from WMAP1.

WML4 is identical to the REF model, except that the mass loading factor is the same as in the MILL simulation, which allows...
us to separate the effects of cosmological parameters and feedback prescriptions.

2.1 Extracting sightlines from the simulations

We use the $z = 2.25$ snapshot, as this is close to the peak in the redshift distribution of the galaxy sample used in R12 ($z \approx 2.36$), and the snapshots of the simulations are saved only every $\Delta z = 0.25$. Although the difference between $z = 2.25$ and $z = 2.36$ is comparable to a change of 3% in $\sigma_8$, in Section 3.1.1 we show that using simulations with different cosmological parameters, with values of $\sigma_8$ differing by 22%, does not lead to significantly different results.

The masses and locations of the dark matter haloes in the simulations are determined using a spherical overdensity criterion as implemented in the SUBFIND algorithm (Springel et al. [2001]). SUBFIND finds the radius, $r_{200}$, and mass, $M_{200}$, of a spherical halo centered on the potential minimum of each identified halo, so that it contains a mean density of 200 times the critical density of the Universe at a given redshift.

We begin by defining a number of halo samples, each characterized by one parameter, the minimum halo mass, $M_{\text{min}}$. Each sample consists of all haloes with $M_h > M_{\text{min}}$. We vary $M_{\text{min}}$ in steps of 0.1 dex between $M_{\text{min}} = 10^{10.5} - 10^{12.5} M_\odot$ and thus consider a total of 20 different halo samples. For each of these samples, we fire 12,500 sightlines through the simulation volume such that each one passes within 5 pMpc of a randomly chosen halo (which ensures that we sample the halo mass function correctly). There are 500 sightlines for every 200 pkpc impact parameter bin. Given that there are, e.g., $\sim 20,000$ haloes with mass above $10^{13} M_\odot$, or $\sim 700$ haloes with mass higher than $10^{12} M_\odot$ in the 100 $h^{-1}$ cMpc box (see Figure 1 for the number densities of haloes above a given mass), a single halo features only once in most distance bins. Although sightlines are always parallel to a side of the box, the axis is chosen randomly. In addition, the position angle with respect to galaxies is also random.

By setting only the minimum halo mass, we implicitly assume that each halo above a given mass limit hosts a galaxy from the observed population. Objects that are potentially missed by the selection based on rest-frame UV colors, e.g. massive red galaxies identified through their rest-frame optical colors (e.g. Franx et al., 2003), have space densities that are more than an order of magnitude smaller than the rest-frame UV selected galaxies used here, and are thus expected to have little impact on our statistics. We verified that using overlapping bins in halo mass with minimum and maximum masses spaced by 1 dex yields very similar results to setting only the lower mass limit. This is due to the shape of the halo mass function, where the typical (median) mass above a given mass limit is only 0.2-0.3 dex higher than the imposed minimum (Figure 1).

The synthetic spectra were created using the package SPECWIZARD written by Schaye, Booth, & Theuns using the procedure described in Appendix A4 of Theuns et al. (1998). The QSO spectra from R12 were taken with Keck/LHRES (Vogt et al., 1994), have a spectral resolution of $\text{FWHM} \approx 5 \text{ km s}^{-1}$, and were rebinned to $2.8 \text{ km s}^{-1}$ pixels. We convolved our simulated spectra with a Gaussian with a $\text{FWHM} = 6.6 \text{ km s}^{-1}$, and rebinned to $1.4 \text{ km s}^{-1}$ pixels. We verified that the results are almost identical if we use the exact match to observed spectra, i.e. $\text{FWHM} \approx 8.5 \text{ km s}^{-1}$, rebinned to $2.8 \text{ km s}^{-1}$, instead of $\text{FWHM} = 6.6 \text{ km s}^{-1}$, and rebinned to $1.4 \text{ km s}^{-1}$ pixels. We added Gaussian noise with a signal to noise (S/N) ratio of 100 to the spectra, which matches the typical S/N of the observations.

Due to uncertainties in the intensity of the ionizing background radiation, it is common practice to scale the optical depth in simulated spectra to match the mean/median absorption level of observed spectra at a given redshift. In order to match the median optical depth in the observed spectra of Rakic et al. (2012), median $\log_{10} \tau_{\text{Ly} \alpha} = -1.27^{+0.03}_{-0.02}$, we select 1000 random sightlines and find the optical depth of all pixels from spectra along those sightlines, from which we then determine the relevant scaling factor. This is done separately for each simulation box used in this study and the same factor is then used for all the spectra drawn from the

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**Table 1.** Numerical parameters. The columns give the comoving size of the box $L$, the total number of particles per component $N$ (dark matter and baryons), the initial baryon particle mass $m_p$, the dark matter particle mass $m_{\text{dm}}$, and the maximum proper gravitational softening length (above $z = 3$ it is fixed in comoving coordinates).

| Simulation | $L$ [$h^{-1}$ cMpc] | $N$ | $m_p$ [$h^{-1}$ $M_\odot$] | $m_{\text{dm}}$ [$h^{-1}$ $M_\odot$] | Max. soft. length [$h^{-1}$ ckpc] |
|------------|----------------------|-----|--------------------------|---------------------------------|-------------------------------|
| L050 N512  | 50                   | 512$^3$ | 1.1 x 10$^7$             | 5.1 x 10$^7$                     | 1                             |
| L100 N512  | 100                  | 512$^3$ | 8.7 x 10$^7$             | 4.1 x 10$^8$                     | 2                             |

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**Figure 1.** Median halo mass above a given minimum halo mass (rising thick colored curves), for different models, as measured from 100 $h^{-1}$ cMpc boxes, with the corresponding 15.9th and 84.1th percentiles (dashed rising curves above and below the median curves). The gray line shows where median halo mass is equal to the minimum halo mass. The declining dotted curves show the corresponding comoving number densities of haloes above a given minimum mass (right y-axis).
corresponding box. The unscaled median optical depths for the different simulations are listed in Table 2. The mean normalized flux in the sample of observed QSO spectra is 0.806. The formula for the effective Lyα optical depth from Schaye et al. (2003) suggests that the mean flux at $z = 2.36$ is 0.802($\pm0.008$), which is consistent with the observations, so we conclude that the IGM probed by the observed QSO sightlines from R12 is representative for the considered redshift.

2.2 Resolution tests

The REF model was run in 25, 50, and 100 $h^{-1}$cMpc boxes, while the rest of the simulations are only available in 25 and 100 $h^{-1}$cMpc boxes. The smallest box size does not contain sufficient high-mass haloes and is therefore not suitable for our study. The 50 $h^{-1}$cMpc simulation box samples the relevant range of the mass function well, and we used this box size to test convergence by comparing it with the 100 $h^{-1}$cMpc box. The latter samples the high-end of the mass function well, but at the low-mass end it resolves haloes with $M_h < 10^{10.5}M_\odot$ with less than $10^2$ dark matter particles (for the simulation with 512$^3$ particles), which is insufficient to robustly identify dark matter haloes (e.g. Jenkins et al. 2001). However, comparison of the REF model with observations suggests that the relevant mass range is $M_h > 10^{11}M_\odot$, which means that 100 $h^{-1}$cMpc simulation boxes are appropriate for our particular problem. We show convergence tests in the Appendix.

3 MEASURING HALO MASSES

In this section we show the results of matching 2-D H I Lyα absorption maps, and 1-D cuts through such maps, to those from the simulations for different minimum halo masses. R12 show 2-D maps of the median H I Lyα optical depth around galaxies, i.e. the optical depth distribution as a function of transverse and LOS separation from galaxies, where distances along the LOS are calculated from velocity separations under the assumption that they are due to the Hubble flow and that there are no peculiar velocities. Given that maps are built by combining many galaxies, in the absence of peculiar velocities the absorption distribution would appear isotropic (assuming the Universe is isotropic in a statistical sense). Therefore, any departure from isotropy in 2-D absorption maps can be attributed to peculiar velocities and/or errors in galaxy redshifts.

R12 used the pixel optical depth method (e.g. Cowie & Songaila 1998, Ellison et al. 2000, Schaye et al. 2000, Aguirre et al. 2002) to recover the H I Lyα optical depth in each pixel of a QSO spectrum. Each galaxy in the field of a QSO is then associated with an array of pixels with varying velocity separation, but at a fixed impact parameter. This is done for each QSO field, and then all the QSO fields are combined to build a galaxy-centered 2-D map, where both transverse and LOS distances are binned logarithmically, and where only absolute LOS velocity difference is taken into account. The simulated maps are built in an analogous way, where instead of galaxies we use dark matter haloes.

For reference, the number of galaxies in the observations per transverse bin depends slightly on the velocity difference (see R12 for details). From small to large impact parameters, the number of galaxies contributing to the 1st (9th) velocity bin is 14 (16), 8 (8), 11 (12), 22 (23), 47 (48), 58 (62), 96 (99), 175 (180), 202 (211).

3.1 Measuring halo mass from 2-D absorption maps

The first panel of Figure 2 shows the observed 2-D H I Lyα absorption map from R12. The remaining panels show, from left to right, maps from simulations for minimum halo masses of $M_{\text{min}} = 10^{10.5}, 10^{11.5}$, and $10^{12.5}M_\odot$. The distance bins in these maps are logarithmically spaced by 0.15 dex, both in the transverse direction and along the LOS. We added errors to the simulated galaxy redshifts, to mimic those from the observations (Steidel et al. 2010), to a random 10% of the simulated redshifts we added errors drawn from a Gaussian distribution with $\sigma = 60\,\text{km}\,\text{s}^{-1}$ (mimicking errors in redshifts measured from nebular emission lines), and to the remaining 90% of redshifts errors with $\sigma = 125\,\text{km}\,\text{s}^{-1}$ (imitating errors measured from rest-frame UV absorption and emission lines).

Haloes with $M_h > 10^{10.5}M_\odot$ produce too little absorption to account for the observed absorption at large impact parameters, while the more massive haloes, $M_h > 10^{11.5}M_\odot$, produce too much absorption in those regions. The third panel, showing absorption near haloes with mass $M_h > 10^{11.5}M_\odot$, resembles the observed distribution most. The observed map is noisier, however, which is not surprising given that hundreds of sightlines contribute to each bin of the simulated maps, compared to $\approx 10$ in the innermost impact parameter bins of the observed map. None of the simulated maps shows enough absorption very close to galaxies (impact parameters $b < 100\,\text{pkpc}$). Steidel et al. (2010) find that the absorption strength keeps rising closer to galaxies using their galaxy-galaxy pairs observations, which sample the $b < 100\,\text{pkpc}$ region well. This suggests that there may be a true deficiency of high column gas close to galaxies in the simulations and that the discrepancy may not only be a result of small number statistics (there are only 15 galaxies in the first, and 8 in the second impact parameter bin of Rakic et al. 2012). We will come back to this question in more detail below.

Figure 2 indicates the approximate mass range for which host haloes produce absorption comparable to the observations. More quantitatively, we estimate the minimum halo mass by minimizing the reduced $\chi^2$ between the observed 2-D Lyα absorption maps and maps from the simulations, taking into account errors on observed data points. We use only regions of maps with LOS separations smaller than 616 km s$^{-1}$ because the absorption signal is consistent with noise beyond this point (see Figure 2). Different distance bins in 2-D maps are uncorrelated in the transverse direction, but they are correlated on scales of 200 km s$^{-1}$ along the LOS (R12). We therefore use 1000 bootstrap realizations of the observed galaxy sample to estimate the errors on the halo mass, instead of using a $\Delta \chi^2$ criterion. For each bootstrap realization of the data, we find the implied minimum halo mass by comparing the resulting maps to the simulated maps, and then find the 1 and 2$\sigma$ confidence intervals from the sample of bootstrap realizations. Given a grid of minimum halo masses spaced by 0.1 dex, the errors on halo masses take discrete values. we set the minimum error to half the grid spacing, i.e. 0.05 dex, since we cannot determine errors to better than this value.

For the 50 $h^{-1}$cMpc REF simulation the implied mass is $\log_{10}M_{\text{min}}/M_\odot = 11.2^{+0.5}_{-0.3}$ (the first and second pairs of errors indicate $\sigma$ and 2$\sigma$ confidence intervals, respectively). For the 100 $h^{-1}$cMpc box it is $\log_{10}M_{\text{min}}/M_\odot = 11.2^{+0.3}_{-0.2}$. The two simulations give almost identical results, which justifies using larger boxes for the rest of the models (see also the Appendix). This also suggests that our mass measurements are not affected by cosmic variance due to the use of a single simulation realization.
Because uncertain baryonic physics and redshift errors could affect the absorption signal close to galaxies, we also restrict the comparison to those parts of the maps where these uncertainties are expected to have a smaller impact. We test two cases where we compare two different velocity separations (e.g. Figure 2), and given the uncertain baryonic physics in the vicinity of galaxies, we choose to compare absorption distributions (as observed by Rakic et al. 2012, their Figure 5), and in the REF simulations near haloes with $M_{\text{min}} > 10^{10.5}$ (using the 50 $h^{-1}$ cMpc box), $10^{11.5}$ (using the 50 $h^{-1}$ cMpc box) and $10^{12}$ $M_{\odot}$ (using the 100 $h^{-1}$ cMpc box) at $z = 2.25$. Redshift errors (as described in the text) were included in the simulated maps. In comparison with the observed absorption map, the second panel shows too little absorption at large impact parameters, while the fourth panel shows too much absorption in those regions.

Table 2. List of main physics variations employed in the used models and an unscaled median optical depth for each simulation.

| Models   | Box size [$h^{-1}$ cMpc] | Description                        | $\log_{10}\tau_{Ly\alpha}$ |
|----------|--------------------------|------------------------------------|----------------------------|
| REF      | 100                      | Reference model                    | -1.34                      |
| REF      | 50                       | Reference model                    | -1.40                      |
| AGN      | 100                      | Includes AGN                       | -1.37                      |
| MILL     | 100                      | Millennium simulation cosmology, $\eta = 4$ (twice the SN energy of REF) | -1.48                      |
| WML4     | 100                      | Wind mass loading $\eta = 4$ (twice the SN energy of REF) | -1.35                      |

Figure 2. Median 2-D distribution of H I Ly$\alpha$ absorption around galaxies, from left to right, as observed by Rakic et al. (2012, their Figure 5), and in the REF simulations near haloes with $M_{\text{min}} > 10^{10.5}$ (using the 50 $h^{-1}$ cMpc box), $10^{11.5}$ (using the 50 $h^{-1}$ cMpc box) and $10^{12}$ $M_{\odot}$ (using the 100 $h^{-1}$ cMpc box) at $z = 2.25$. Redshift errors (as described in the text) were included in the simulated maps. In comparison with the observed absorption map, the second panel shows too little absorption at large impact parameters, while the fourth panel shows too much absorption in those regions.
used this simulation to show that AGN eject large amounts of gas from the haloes at $z \sim 2 - 3$, which may explain why we need to move to higher mass haloes to get high enough columns of neutral gas to account for the observed absorption. Nevertheless, given that the results differ by only 0.3 dex and by less than 1σ, we conclude that our method for measuring halo mass is sufficiently robust to changes in the baryonic physics prescriptions.

To quantify the impact of cosmology on our results, we compare the MILL and WML4 simulations, which use the same subgrid physics and differ mostly in terms of $\sigma_s$, which is 0.9 for the former and 0.74 for the latter model. We find minimum halo masses of $\log_{10}M_{\text{min}}/M_\odot = 11.7_{-0.40}^{+0.50}+0.30$ and $11.4_{-0.10}^{+0.50}+0.80$ for MILL and WML4, respectively. These estimates are consistent with each other and with the value implied by the REF model. The fact that WML4 gives a result consistent with that for the MILL model, suggests that the exact value of $\sigma_s$ does not change the measured value of the halo mass significantly.

This result also suggests that the fact that we compared the $z = 2.25$ simulation snapshot with observations at $z = 2.36$ should not have any significant effect on our result. The difference in redshift corresponds to a slight change in $\sigma_s$, and we have shown that the exact value of this parameter does not change the results significantly.

For comparison, we show 2-D Ly$\alpha$ absorption maps for different models in Figure 4 for haloes with $M_h > 10^{11.5} M_\odot$. Model AGN shows weaker absorption within $\sim 300$ kpc from galaxies in comparison with the other models and WML4 shows less absorption relative to the REF model.

The implied minimum masses from all models are summarized in Table 3 and Figure 5. All models are consistent with each other at the 1σ level. It is thus clear that the statistical errors on the minimum halo mass, which are around 0.2-0.3 dex, are comparable to or larger than the systematic errors arising due to uncertainties in the physics important for galaxy formation, as inferred from simulations with different feedback prescriptions and different cosmologies. This demonstrates the robustness of this method for measuring halo masses. We also list the reduced $\chi^2$ values between the observed map and the best matching simulated maps in the considered region, i.e. for impact parameters 0-2 pMpc and velocity separations 154 - 616 km s$^{-1}$, with the caveat that the distances bins are correlated along the LOS on the $\sim 1$ pMpc scale (R12).

### Table 3. The minimum halo masses (with 1 and 2σ confidence intervals) of the $(z) \approx 2.36$ star-forming galaxies of R12 inferred from a comparison of the observed HI absorption around them to predictions from different hydrodynamical simulations. Only impact parameters 0-2 pMpc and velocity separations 154 - 616 km s$^{-1}$ are considered. The corresponding number densities of haloes (and 1 and 2σ confidence intervals) as measured from the simulations with 100 h$^{-1}$ cMpc boxes are presented in the third column. For reference, the observed number density of galaxies in the photometric sample, from which the objects in R12 were drawn for spectroscopic follow-up, is $11 \times 10^{-3} h^3$ cMpc$^{-3}$, with an uncertainty of 10% (Reddy et al. 2008). The last column shows the reduced $\chi^2$ between the observed map and the best matching simulated map, for impact parameters 0-2 pMpc and velocity separations 154 - 616 km s$^{-1}$.

| Models     | Min. halo mass $[\log_{10}M_\odot]$ | $n [10^{-3} h^3$ cMpc$^{-3}$] | Red. $\chi^2$ |
|------------|-------------------------------------|-------------------------------|---------------|
| REF        | $11.6_{-0.20}^{+0.50}+0.60$          | $2.9_{-1.2}^{+1.3}+2.2$       | 1.018         |
| AGN        | $11.9_{-0.30}^{+0.50}+0.70$          | $1.7_{-0.5}^{+0.7}+3.7$       | 0.934         |
| MILL       | $11.7_{-0.40}^{+0.50}+0.90$          | $4.1_{-0.5}^{+0.7}+3.3$       | 0.989         |
| WML4       | $11.4_{-0.10}^{+0.50}+0.80$          | $4.7_{-0.5}^{+1.1}+3.5$       | 1.091         |

### 3.1.2 Number densities of haloes

The number density of galaxies in the photometric sample, from which the galaxies in R12 were drawn, is $11 \times 10^{-3} h^3$ cMpc$^{-3}$, with an uncertainty of 10% (Reddy et al. 2008). The largest weights for spectroscopic follow-up were given to objects in the apparent magnitude range $R = 23 - 24.5$ (Steidel et al. 2004), while the limit for the photometric sample is $R = 25.5$. In addition, objects near the QSO sightlines (i.e. within 1-2 arcminutes) were given extra weight. There are $\sim 2.5$ times more objects in the photometric sample for the limiting magnitude of $R = 25.5$ than for $R = 24.5$, and so the lower limit on the number density of galaxies in the spec-
Halo mass from Lyα absorption profiles

3.1.3 Comparison with estimates from clustering measurements

Estimates of halo masses of $z \sim 2$ star-forming galaxies were recently presented by Conroy et al. (2008) and Trainor et al. (2012). As already discussed in the introduction, using a clustering analysis, Conroy et al. (2008) found the minimum halo mass to be $10^{11.15} M_\odot$ for the WMAP year-1 cosmology, and 0.3-0.4 dex smaller (i.e. $10^{11.15} - 0.3$ dex) for the WMAP year-3 cosmology (which is the default cosmology in our study). Trainor & Steidel (2012) measure masses of $M_h > 10^{11.7} M_\odot$ for the spectroscopic sample using WMAP year-7 cosmological parameters (where $\sigma_8$ is intermediate between those from WMAP year-1 and year-3, while the value for $\Omega_m$ is closer to that from WMAP year-1). Our results for the models that use WMAP year-1 and year-3 cosmological parameters ($\log_{10} M_{\text{min}}/M_\odot = 11.7 \pm 0.30$ for the MILL model which uses WMAP1, and 11.4 $\pm 0.30$ for the WML4 model which uses WMAP3), are in good agreement with these estimates. We conclude that the two methods (i.e. clustering analysis and matching of the Lyα absorption profiles) give consistent results.

3.1.4 Measuring mass from pencil beam surveys

We have demonstrated that comparisons of observed 2-D Lyα absorption maps around galaxies with maps extracted from cosmological, hydrodynamical simulations can be used to measure the halo masses of the galaxy population in question. Our observed QSO-galaxy fields typically span areas of $\sim 5 \times 7$ arcminutes with the QSO in the middle. Here we test the performance of the method for a limited survey area of only $\sim 30 \times 30$ arcseconds, which corresponds to a cut along the LOS through the first impact parameter bin of the above 2-D maps ($b \lesssim 100$ pkpc and velocity separation $154 < v_{\text{LOS}} < 616$ km s$^{-1}$). The implied minimum halo mass is $\log_{10} M_{\text{min}}/M_\odot = 11.6_{-0.30}^{+0.50}$, which agrees very well with that inferred from a comparison of the full maps ($\log_{10} M_{\text{min}}/M_\odot = 11.6_{-0.20}^{+0.40}$), also in terms of the size of the error bars.

This finding is relevant for future galaxy-QSO pair surveys such as the one planned with the VLT/MUSE integral field spectrograph (Bacon et al. 2010), whose field of view is $1 \times 1$ arcminute. Applying this method to MUSE observations will allow estimates of halo masses of Lyα emitters from a single telescope pointing on each QSO in the survey. This eliminates the need to make a wide field mosaic to measure clustering, which would be too expensive for the faint objects dominating the number density of galaxies detected in the deep fields.

4 REDSHIFT SPACE ANISOTROPIES

R12 reported two types of redshift space anisotropies in the observed 2-D Lyα absorption maps. At small impact parameters ($\lesssim 200$ pkpc) the absorption signal is elongated along the LOS, which is likely a result of gas peculiar velocities of $\approx 200$ km s$^{-1}$, and errors in galaxy redshifts ($\approx 125$ km s$^{-1}$). On the other hand, at large separations from galaxies ($\approx 1.5$ pkpc) the absorption appears compressed along the LOS, which R12 attributed to large-scale gas infall into the potential wells populated by the observed galaxies.

Here we use simulated observations to examine the origin of the observed redshift space anisotropies. Figure 6 shows 2-D absorption maps centered on haloes with masses higher than the minimum mass inferred in the previous section, i.e. $M_h > 10^{11.5} M_\odot$ (for 4 cases: $i$) the default case, i.e. redshift errors with $\sigma = 60$ km s$^{-1}$ for 10% of galaxy redshifts, and $\sigma = 125$ km s$^{-1}$ for the remaining 90% of redshifts, and taking into account peculiar velocities, $ii$) no redshift errors, $iii$) ignoring peculiar velocities, and $iv$) a number of galaxies per impact parameter bin identical to the observations of R12.

Comparing the 2nd and 3rd panels of Figure 6 we see that the effect of redshift errors is to wash out the signal along the LOS. The 4th panel shows the case where we ignore peculiar velocities. At small impact parameters ($\lesssim 200$ pkpc), the absorption...
is much reduced, demonstrating that peculiar velocities strongly enhance the small-scale absorption excess. In addition, on large scales ($\lesssim 1.5$ pMpc) the absorption enhancement is now much more isotropic, demonstrating that the observed large-scale ($\gtrsim 1.5$ Mpc) compression along the LOS is likely due to large-scale infall. The observations of R12 are the first of gas infall into large-scale potential wells. We just note here that, as expected, ignoring both peculiar velocities and redshift errors results in a map with axisymmetric absorption (not shown).

In the 5th panel we use the same number of sightlines per impact parameter bin as in the observations. The resulting map is noisier in comparison with the previous panels with simulated maps, but the redshift space distortions seen in the first panel are also clearly visible in this panel.

A more quantitative comparison is provided by Figures 7 and 8 which show cuts through these maps along the LOS and in the transverse direction, respectively, for three different cases. The top left panel of Figure 7 makes it very clear that the simulations underpredict the amount of absorption for impact parameters smaller than $\approx 100$ pkpc for velocities $\lesssim 154$ km s$^{-1}$. Conversely, at impact parameters $0.13-0.25$ pMpc the simulations overestimate the absorption for velocities $\lesssim 154$ km s$^{-1}$. However, the number of observed galaxies in these two impact parameter bins is too small (15 and 8, respectively) to obtain an accurate estimate of the significance of these discrepancies. Note also that a simple $\chi^2$ test would strongly overestimate the significance of these discrepancies because the points are strongly correlated in the LOS direction (R12).

Both figures show that redshift errors smooth the signal along the LOS on scales $\lesssim 10^2$ km s$^{-1}$. The orange dashed curves, which do not take peculiar velocities into account, lie below the default case (solid black curves) for velocity separations $\lesssim 150$ km s$^{-1}$, and above them at larger velocity separations. The increased optical depth closer to galaxies could be due to large-scale infall of gas enhancing absorption through "filling" in redshift space. Another possibility is that the enhanced absorption is due to lines getting broadened due to large-scale galactic outflows, which could also significantly affect our median statistics.

Comparing the bottom-right panels of Figures 7 and 8 which show the absorption for large impact parameters and large velocity separations, respectively, we see that the absorption is observed to be stronger along the LOS (i.e. in Figure 7) than transverse to the LOS (i.e. in Figure 8). The simulations show the same anisotropy (compare solid black curves in the bottom-right panels of Figures 7 and 8), and the anisotropy is enhanced when redshift errors are ignored (dotted blue curves). In contrast, when peculiar velocities are ignored (dashed orange curves) the LOS and transverse directions are consistent with each other. Thus, the simulations support the interpretation of R12 of the large-scale anisotropy as being due to infall.

In Figure 8 we add different amounts of scatter to the galaxy redshifts. Large redshift errors smooth the absorption signal more along the LOS. The last panel shows the case with redshift errors of $\sigma = 300$ km s$^{-1}$, where instead of compression along the LOS relative to the direction transverse to the LOS, we see elongation. This suggests that the errors in galaxy redshifts have to be $< 200$ km s$^{-1}$ to study large-scale infall of gas into the potential wells of star-forming galaxies.

5 SUMMARY & CONCLUSIONS

Observations have shown that the absorption of the light from background QSOs is enhanced at the rest-frame wavelength of H I Ly$\alpha$ when a sightline passes within several pMpc from a galaxy. We compared the observed median Ly$\alpha$ absorption profiles around star-forming galaxies at $z \approx 2.36$ from Rakic et al. (2012) with predictions from cosmological SPH simulations in order to statistically constrain the total masses of the haloes hosting the observed galaxy population, and to explain the observed redshift space distortions. We confined our comparison to transverse separations $0-2$ pMpc and to LOS velocity differences $154 - 616$ km s$^{-1}$. The large-scale cut avoids comparing regions without signal and the small-scale cut excludes the region most affected by redshift errors and uncertain physical processes.

The most important conclusions of this study are:

- Using the REFL model from the OWLS suite of simulations, we derive a minimum halo mass of $M_{\text{halo}}/M_{\odot} = 11.6^{+0.50}_{-0.26} - 0.60$, where the first and second pairs of errors indicate the 1 and 2$\sigma$ uncertainties, respectively. This is in good agreement with the estimates from the clustering analyses of Conroy et al. (2008) and Trainor et al. (2012) performed on the same galaxy population.
- This method is robust to changes in feedback prescriptions as demonstrated by comparison with the AGN model in which galaxies eject large amounts of gas at the redshift of interest here.

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Figure 7. Cuts along the LOS through the panels of Figure 6 (\(M_h > 10^{11.5} M_\odot\)). The gray symbols show the observations of R12. The horizontal dashed line indicates the median optical depth of all pixels. Black solid curves show the default case (includes errors in galaxy redshifts, and takes peculiar velocities into account), blue dotted curves show the results without redshift errors, and orange dashed curves the case where peculiar velocities are ignored. Please note that the mass measurement above is done by comparison of the observed and simulated maps for the LOS separations of 154-616 km s\(^{-1}\), while this figure extends only to 436 km s\(^{-1}\).

The implied minimum mass of log\(_{10} M_{\text{min}}/M_\odot = 11.9^{+0.20}_{-0.30} + 0.30_{-0.40} - 0.70\), although 0.3 dex higher, is consistent with the REF model within 1\(\sigma\).

- The minimum halo mass inferred from a comparison with the MILL simulation (log\(_{10} M_{\text{min}}/M_\odot = 11.7^{+0.05}_{-0.30} + 0.40_{-0.10} - 0.20\)) is consistent with that required by the WML4 model (log\(_{10} M_{\text{min}}/M_\odot = 11.4^{+0.50}_{-0.10} + 0.80\)). As these two models assume different cosmologies (WMAP year-1 vs. WMAP year-3), but are otherwise identical, this suggests that the method is not very sensitive to differences in cosmological parameters.

- If we consider only impact parameters \(\lesssim 100\) pkpc and LOS velocity differences 154 – 616 km s\(^{-1}\), then we infer a mass of log\(_{10} M_{\text{min}}/M_\odot = 11.6^{+0.40}_{-0.05} + 0.50_{-0.10} - 0.70\), which is almost identical to the one obtained from the full 2-D map (impact parameters \(< 2\) pMpc). This is very encouraging for future narrow field QSO-galaxy surveys (e.g. the one planned with the VLT/MUSE), where one will be able to estimate halo masses of Ly\(\alpha\) emitters with a single telescope pointing, without the need for a wide field mosaic.

- The observed elongation of the absorption signal of \(\approx\)
200 km s\(^{-1}\) at small impact parameters is a product of uncertainties in galaxy redshifts, observed to be \(\approx 125\) km s\(^{-1}\), and the peculiar motions of gas in and around galaxy haloes.

- At impact parameters < 0.13 pMpc the simulations may under-predict the absorption for velocities < 154 km s\(^{-1}\). Conversely, at impact parameters 0.13-0.25 pMpc the simulations may over-predict the absorption in the same velocity range. However, the number of observed galaxies in these two impact parameter bins is too small (15 and 8, respectively) to estimate the significance of these discrepancies.

- The compression of the signal on large scales (\(\gtrsim 1.5\) pMpc) is a result of gas infall into the potential wells occupied by the galaxies. To observe this infall, the accuracy of galaxy redshifts has to be significantly better than 200 km s\(^{-1}\), as larger redshift errors smooth the absorption signal along the LOS, disguising the compression signature.

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Figure 9. Similar to Figure 6, the first panel shows the observations of R12, and in the rest of panels we vary the size of the errors in the galaxy redshifts in the simulations (50 h^{-1} cMpc box, REF simulation): $\sigma = 0$ (the median optical depth at small impact parameters exceeds the scale maximum, and appears black), 100, 200, and 300 km s^{-1}, from left to right. Adding errors with $\sigma \gtrsim 200$ km s^{-1} masks the large-scale ($\gtrsim 1.5$ pMpc) compression of the absorption distribution along the LOS relative to that transverse to the LOS.

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APPENDIX A: CONVERGENCE TESTS

Figure A1 shows a resolution test for the 50 $h^{-1}$ cMpc REF simulation, performed with $128^3$, $256^3$, and $512^3$ particles. The median log$_{10}(\tau_{Ly\alpha})$ curves as a function of 3-D proper Hubble distance from the galaxies are consistent with each other for all but the highest mass bin. In the highest mass bin (right panel) the resulting curve for the simulation with the poorest resolution is below the curves for the simulations with higher resolution, but the simulations with $256^3$ and $512^3$ particles give consistent results. Therefore, we conclude that the simulation results are converged with respect to the numerical resolution.

Figure A2 compares the results for the 50 $h^{-1}$ cMpc REF simulation with $256^3$, and the 100 $h^{-1}$ cMpc REF simulation with $512^3$ particles. In this case the particle masses in the two simulations are the same, but the simulation volume is changed. The median optical depth curves show that the results are converged with respect to the box size.
Figure A1. Convergence with respect to the numerical resolution: median $\log_{10}(\tau_{\text{Ly}\alpha})$ as a function of proper 3-D Hubble distance from galaxy haloes in the $50\ h^{-1}$ cMpc $REF$ simulations, with $128^3$, $256^3$, and $512^3$ particles. Each panel shows the results for a different halo mass range, as indicated in the panels, while grey symbols with $1\sigma$ and $2\sigma$ error bars show the observations of R12. We added errors to the galaxy positions in simulations to mimic redshift errors (see text for more details).

Figure A2. Convergence with respect to the size of the simulation box: Median $\log_{10}(\tau_{\text{Ly}\alpha})$ as a function of proper 3-D Hubble distance from galaxy haloes in the $50\ h^{-1}$ cMpc $REF$ simulation with $256^3$, and in the $100\ h^{-1}$ cMpc $REF$ simulation with $512^3$ particles. Each panel shows the results for a different halo mass range, as indicated in the panels, while grey symbols with $1\sigma$ and $2\sigma$ error bars show the results from the observations of R12. We added errors to the galaxy positions in simulations to mimic redshift errors (see text for more details).