Tunneling into Multiwalled Carbon Nanotubes: Coulomb Blockade and Fano Resonance

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Tunneling spectroscopy measurements of single tunnel junctions formed between multiwalled carbon nanotubes (MWNTs) and a normal metal are reported. Intrinsic Coulomb interactions in the MWNTs give rise to a strong zero-bias suppression of a tunneling density of states (TDOS) that can be fitted numerically to the environmental quantum-fluctuation (EQF) theory. An asymmetric conductance anomaly near zero bias is found at low temperatures and interpreted as Fano resonance in the strong tunneling regime.

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Coulomb blockade (CB) has been studied intensely in a multi-junction configuration, in which electron tunnel rates from the environment to a capacitively isolated "island" are blocked by the e-e interaction if the thermal fluctuation is below the charging energy $E_c = e^2/2C$ and the quantum fluctuation is suppressed. In the case of a single-junction circuit, the understanding of CB is less straightforward. The Coulomb gap, supposedly less significant for the case of low-impedance environments, should be established only if the environmental impedance exceeds $R_Q$.

In single-walled carbon nanotubes (SWNTs), the reduced geometry gives rise to strong e-e interaction. Indeed, CB oscillations and evidence of Luttinger liquid (LL) have been observed. In contrast to SWNTs, in which only two conductance channels are available for current transport, MWNTs with diameter in the range of $d$=20-40 nm have several tens of conductance channels. The energy separation of the quantized subbands, given by $\Delta E = \hbar v_F / d$, is about 13-26 meV taking the Fermi velocity $v_F = 8 \times 10^5$ m/s. This value is about an order of magnitude smaller than that of SWNTs. Experiments indicate that MWNTs are considerably hole-doped, thus a large number of subbands, on the order of ten, are occupied. Observations of weak localization, electron phase interference effect, and universal conductance fluctuations support the view that low frequency conductance in MWNTs is contributed mostly by the outmost graphene shell and is characterized by 2D diffusive transport. In addition to the phase interference effects, a strong e-e interaction has also been observed in MWNTs. Pronounced zero-bias suppression of the TDOS has been observed several times in the tunneling measurements. Moreover, the TDOS shows a power-law, i.e., $\nu(E) \sim E^n$, which resembles the case of a LL. It is noteworthy that in the EQF theory, for a single tunnel junction coupled to high-impedance transmission lines, such a scaling behavior is also predicted at the limit of many parallel transmission modes. The physical origin of these power laws is the linear dispersion of bosonic excitations that are characteristic both for LL, which is a strictly 1D ballistic conductor, and a single tunnel junction connected to a 3D disordered conductor. In the latter case, the quasiparticle tunneling is suppressed at $V \ll e/2C$, therefore the charge is transported with 1D plasmon modes. The fact that MWNTs have many conductance modes, together with the observation of a crossover from power-law to Ohmic behavior at higher voltages, suggests that the EQF theory is more appropriate to describe the observed TDOS renormalization. However, most of these measurements were done in multi-junction configurations. A single tunnel junction measurement is needed to further clarify this issue.

In this Letter, millimeter-long CVD-grown MWNTs are measured by a cross-junction method. The MWNT samples are composed of loosely entangled nanotubes of diameters between 20 to 40 nm that are roughly parallel to each other and up to 2 mm long. The single tunnel junctions are formed by crossing a very thin (<1μm) MWNT bundle with a narrow strip of metal wire fabricated on an insulating substrate. We explored different electrode materials including Au, Cu, Sn, and Al. In the case of Sn and Al, a small magnetic field is applied to suppress the superconducting state below $T_c$. No obvious change of device characteristics attributable to the choice of metals is observed. With such a cross-junction configuration the measured conductance is contributed exclusively by the tunnel junction, since the current is passed along one arm of the MWNT/metal and the voltage is measured along the other, non-current carrying arm. Thus the device can be understood as a small number of single junctions in parallel. Despite the simplicity of their fabrication, we find that the devices are very stable and sustain several cooling cycles without apparent change of characteristics. More than 20 samples are measured, all yielding strong zero-bias suppression of the TDOS.

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The current $I(V)$ and $G \equiv dI/dV$ are calculated by a golden-rule approach incorporating the environmental influence by $P(E)$, the probability for a tunneling electron to lose energy to the environment. $P(E)$ can be calculated from its Fourier transform, the phase correlation function $J(t)$. In the transmission-line model, $J(t)$ is determined by the total environmental impedance $Z(t) = (iωC + Z^{-1}(ω))^{-1}$, where $Z(ω)$ is the external environmental impedance. We apply the method in Ref. 9 to evaluate $P(E)$ from an integral equation without the need of going to the time domain. The I-V characteristics are then calculated for finite temperatures and arbitrary junction impedance. The parameters that appear in the numerical calculation are the damping strength $\alpha = Z(0)/RC$, the inverse relaxation time $\omega_RC$, and the quality factor $Q = \omega_RC/\omega_S$ with the resonance frequency of the undamped circuit $\omega_S = (LC)^{-1/2}$. It is noted that the quality factor $Q$ plays only a minor role as an additional adjustable parameter. Therefore it is not important to the fit, and is always set to unit.

We then try to fit our experimental data with the EQF theory. Since $E_C$ and $R_t$ are determined by the high-voltage data, the isolation resistance $R_{iso} = Z(0)$ is the only adjustable parameter in our fitting. In contrast to the case of Ref. 11, where $R_{iso}$ is formed by ideal Ohmic and temperature-independent resistors, $R_{iso}$ in our case are provided by the resistive impedance of the MWNTs themselves, which should be temperature-dependent. Indeed, from the fitting, we see an evolution of $\alpha$ from 0.1 at 20 K to 0.25 at 1-4 K and then $\alpha$ saturates (Fig. 1c).

Note that dimensionless units are used with $G$ normalized by $1/R_t$ and voltage normalized by $e/2C$. Therefore the number of the single tunnel junctions has no effect on the fitting, and our measurements of different samples can be directly compared. We find that for different samples with scattered characteristics (see Table I), at low temperatures the exponent $\alpha$ reaches a universal value of $0.25-0.35$, which agrees with previous multi-junction measurements. It yields $R_{iso} = 3.3-4.6$ kΩ, which is roughly a constant for different samples. This coincidence is not accidental but reflects the intrinsic electrodynamic modes of the MWNTs, which can be modelled as an ideal resistive LC transmission line: $R = (L'/C')^{1/2}$ with the kinetic inductance estimated as $L' = R_Q/2NV_f \approx 1$ nH/µm for $N \approx 10-20$ modes and the capacitance $C' \approx 20-30$ aF/µm. Therefore, the “environment” with respect to the single-junctions in our devices is provided by MWNTs themselves, not by the external circuits.

![FIG. 1: (a) $dI/dV$ as a function of $V$ in dimensionless units measured at $T = 0.12$, 0.25, 0.78, 1.2, 1.7, 4.5, 10, 20 K (sample 990530s6, curves are offset for clarity). Dashed lines are the fits of EQF theory. (b) DC current simultaneously at 20 K to 0.25 at 1-4 K and then $\alpha$ from 0.1 at 20 K to 0.25 at 1-4 K and then $\alpha$ saturates (Fig. 1c).

**TABLE I: A partial list of characteristics of the samples.**

| Sample  | $R_t$ (kΩ) | $E_C$ (eV) | $C$ (aF) | $R_{iso}$ (kΩ) | $\alpha$ |
|---------|------------|------------|---------|----------------|---------|
| 990316  | 18.4       | 0.019      | 4.2     | 3.3$^a$        | 0.25$^a$|
| 990320  | 48.3       | 0.014      | 5.7     | 3.3$^a$        | 0.25$^a$|
| 990530s6| 8.6        | 0.01       | 8.0     | 3.3$^a$        | 0.25$^a$|
| 990530s6| 10.0       | 0.02       | 4.0     | 4.6$^a$        | 0.35$^a$|
| 990202  | 9.1        | 0.004      | 20.0    | 3.5$^a$        | 0.27$^a$|

$^a$value acquired at $T = 1.2-4.3$ K.
FIG. 2: Scaled conductance $G(V,T)/G(0,T)$ of another sample (990202). The inset shows the original $dI/dV$ vs. $V$ with the dashed line calculated with exponent $\alpha = 0.27$.

modifies the tunneling spectra. Unlike the case of a two-junction configuration, where the electrons are confined by the two contacts if the nanotube is clean enough, in a single-junction configuration the electrons can be confined by disorders when the MWNTs are “dirty”, such that the impedance of the local environment of the junction is larger than $R_Q$. A stacking mismatch between adjacent walls and other structural imperfections are possible sources of disorders in MWNTs, resulting in discrete energy levels.

By cooling down the devices to below 1 K, we observe that $G$ develops a narrow resonance-like anomaly at very low bias (Fig. 3). The asymmetric anomaly builds up consistently as temperature decreases and even shows a dip structure. The line shape resembles that of a Fano resonance.

Unlike the Coulomb structure, which is caused by static e-e interaction, a Fano resonance arises from an e-e exchange interaction between two interfering scattering channels: a discrete energy level and a continuum band. It has recently been rediscovered in mesoscopic systems such as semiconductor quantum dots, SWNTs, etc. [13]. Taking a quantum dot as an example, it can be considered as a gate-confined droplet of electrons with localized states. The coupling of the dot to the leads can be tuned to control the system to enter different transport regimes: If the dot is weakly coupled with the environment, a well-established CB develops. The charge transport is suppressed except for narrow resonances at charge degeneracy points. When the tunnel barriers become more transparent, the dot enters the Kondo regime – i.e., below a characteristic Kondo temperature $T_K$, spin-flip co-tunneling events introduce a narrow symmetric TDOS peak at $E_F$ that can be interpreted as a discrete level. If the coupling is strong enough, the interference between this discrete level and the conduction continuum gives rise to an asymmetric resonance. In Ref. [13], such a crossover from a well-established CB through Kondo regime to Fano regime has been clearly observed.

We find that the asymmetric resonance curve of $G$ can be fitted by the Fano’s formula: $G \sim (e + q)^2/(e^2 + 1)$. Here $q$ is the so-called asymmetry parameter, $e = (eV - \varepsilon_0)/\gamma$ is the dimensionless detuning from resonance, and $\gamma$ is the FWHM of the resonance. As expected, the asymmetric parameter $q$ as a measure of the degree of coupling between the discrete state and the continuum increases when the temperature drops.

The Kondo temperature, estimated from the relation $\gamma = 2k_B T_K$, is consistent for each device at different temperatures, and agrees with the observed FWHM of the resonance. If Kondo physics truly exists, then $G$ at voltages near the resonance should show non-monotonic temperature dependence around $T_K$ [15]. Indeed, the $G−V$ curves in Fig. 3 exhibit such behavior: $G$ at the peak position first drops with $T$ and then rises up below $\sim 1$ K (plotted in Fig. 4b). Moreover, we find that a perpendicular magnetic field gives rise to effects that are two-fold (Fig. 4a and 4c): First, the background conductance increases monotonically with the applied $B$. Second, the dip seen at zero field gradually disappears and the resonance turns into a nearly symmetric peak at high field, similar to the pattern observed in semiconductor quantum dots [13].

The magnetic field effect can be explained as follows: First, adding a flux should change the amplitude and/or the phase for the resonant channels and therefore break down the coherent backscattering and increase the forward transmission through the channel. Second, the magnetic field can destroy the interference between the

| Sample   | $T$ (K) | $q$  | $\varepsilon_0$ (meV) | $\gamma$ (meV) | $T_K$ (K) |
|----------|---------|------|-----------------------|----------------|----------|
| 990530s6 | 0.25    | 0.58 | 0.43                  | 0.32           | 1.86     |
| 990530s6 | 0.12    | 1.75 | 0.57                  | 0.29           | 1.68     |
| 990530s1 | 0.25    | 0.92 | 0.3                   | 0.65           | 3.77     |
| 990530s1 | 0.08    | 1.97 | 0.43                  | 0.56           | 3.25     |

TABLE II: Characteristics of the two samples in Figure 3.
FIG. 4: (a) The dependence of zero-bias $dI/dV$ on perpendicular magnetic field. (b) The temperature dependence of $dI/dV$ measured at different voltages. (c) Effect of perpendicular magnetic field. From bottom to top: $B = 0, 1, 3, 6$ Tesla (sample 990530s6).

resonant and nonresonant paths, transforming a resonant dip into a peak.

Since Kondo physics is historically interpreted as the interplay between the d-orbitals of magnetic impurities and the conduction continuum, we have to eliminate the possibility that the observed Fano resonance comes from residual traces of the Fe/Si catalyst in the MWNT samples. It has been shown that magnetic impurities in MWNTs cause an enhancement of thermoelectric power [17], which is absent in our careful TEP measurements [18]. Furthermore, no Fe signature can be detected in the body of the MWNT bundles within the instrumental resolution in the energy dispersion X-ray and TEM studies. Therefore the observed Fano resonance must be an inherent property of MWNTs, which can be virtually treated as quantum dots strongly coupled to the leads. We noticed that recently Buitelaar et al. have also seen clear traces of CB and Kondo resonance in MWNT SET devices [19]. Their observed Kondo temperature $T_K = 1.2$ K is in good agreement with our results.

In summary, strong zero-bias suppression of the TDOS is observed in MWNTs’ single tunnel junctions that can be explained well by the EQF theory. The observed exponent $\alpha \approx 0.25–0.35$ is found to be consistent for all the samples. Similar to the case of an open quantum dot, in low-impedance junctions we find that a Fano-resonance-like asymmetric conductance anomaly builds up below mV energy scales. It seems that MWNTs provide us a good laboratory to study the interplay between strong e-e interaction and disorder scattering.

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