The discovery of a very cool, very nearby brown dwarf in the Galactic plane

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ABSTRACT
We report the discovery of a very cool, isolated brown dwarf, UGPS 0722-05, with the UKIDSS Galactic Plane Survey. The near-infrared spectrum displays deeper H₂O and CH₄ troughs than the coolest known T dwarfs and an unidentified absorption feature at 1.275 µm. We provisionally classify the object as a T10 dwarf but note that it may in future come to be regarded as the first example of a new spectral type. The distance is measured by trigonometric parallax as \( d = 4.1^{+0.6}_{-0.5} \) pc, making it the closest known isolated brown dwarf. With the aid of Spitzer/IRAC we measure \( H-[4.5] = 4.71 \). It is the coolest brown dwarf presently known – the only known T dwarf that is redder in \( H-[4.5] \) is the peculiar T7.5 dwarf SDSS J1416+13B, which is thought to be warmer and more luminous than UGPS 0722-05. Our measurement of the luminosity, aided by Gemini/T-ReCS \( N \) band photometry, is \( L = 9.2 \pm 3.1 \times 10^{-7} L_\odot \). Using a comparison with well studied T8.5 and T9 dwarfs we deduce \( T_{\text{eff}} = 520 \pm 40 \) K. This is supported by predictions of the Saumon & Marley models. With apparent magnitude \( J = 16.52 \), UGPS 0722-05 is the brightest brown dwarf discovered by UKIDSS so far. It offers opportunities for future study via high resolution near-infrared spectroscopy and spectroscopy in the thermal infrared.

Key words: surveys - stars: low mass, brown dwarfs

1 INTRODUCTION

In the past 15 years \( \sim 200 \) T dwarfs, have been discovered in the local field with the Two Micron All Sky Survey (2MASS), the Sloan Digital Sky Survey and the United Kingdom Infrared Telescope Deep Sky Survey (UKIDSS), see e.g. Burgasser et al. (2002); Leggett et al. (2000); Burningham et al. (2010a). These discoveries are useful for investigating the substellar mass function. Searches in young clusters e.g. Lodieu et al. (2007); Weights et al. (2009); Luhman (2004) suggest that the ratio of brown dwarfs to stars is between \( \sim 1:6 \) and \( \sim 1:3 \) (excluding companions) but there are growing indications that fewer exist in the local field (e.g. Burningham et al. 2010a). The nearest isolated brown dwarfs known until now (LP944-20, DENIS-P J025503.5-470050, DENIS J081730.0-615520) are located at distances \( d = 4.9-5.0 \) pc from the Sun (Artigau et al.2010; Tinney 1998; Costa et al. 2006). These are the 46th, 48th and 49th nearest systems. If the mass function in the local field is similar to that in young clusters then we should expect that some brown dwarf primaries remain undiscovered at \( d < 5 \) pc.
Most such objects would have types $\geq$T8.5 in order to lie below the 2MASS detection limit (Skrutskie et al. 2006).

The UKIDSS Large Area Survey (LAS, Lawrence et al. 2007) has discovered several brown dwarfs cooler than those found by 2MASS (e.g. Warren et al. 2007; Burningham et al. 2008 [hereafter B08]; 2010b). The CFHT Brown Dwarf Survey has yielded two similar discoveries (e.g. Delorme et al. 2008). Most of these objects have been classified as T8.5 or T9 dwarfs because the broad H2 band. 2008). Most of these objects have been classified as T8.5 or T9 dwarfs because the broad H2 band.

The CFHT Brown Dwarf Survey has yielded two similar discoveries (e.g. Delorme et al. 2008; Warren et al. 2007; Burningham et al. 2007) has discovered several brown dwarfs cooler than those of T8 dwarfs. The slight differences in the spectra belie a large drop in effective temperature from 700-800 K at T8 to 500-600 K for the coolest objects (B08; Leggett et al. 2010a, hereafter L10a). Here we report the discovery in the UKIDSS Galactic Plane Survey (GPS, Lucas et al. 2008, hereafter L08) of UGPS J072227.51-054031.2 (hereafter UGPS 0722-05), an even cooler and less luminous brown dwarf. The GPS has found by 2MASS (e.g. Warren et al. 2007; Burningham et al. 2007) has discovered several brown dwarfs cooler than those of T8 dwarfs. The slight differences in the spectra belies a large drop in effective temperature from 700-800 K at T8 to 500-600 K for the coolest objects (B08; Leggett et al. 2010a, hereafter L10a).

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## 2 CANDIDATE SELECTION

UGPS 0722-05 was identified as the only good candidate late-T or Y dwarf amongst the 604 million sources in GPS 6th Data Release to satisfy the colour criteria $J-H<0.2$ mag, $H-K<0.1$ mag. We used several data quality restrictions to minimise the number of false candidates (see L08). The criteria were: $jmhPotErr<0.3$, $hmrPotErr<0.3$ (limiting the uncertainty in source colours); $jppErrBits<256$, $hppErrBits<256$, $k_jppErrBits<256$ (removes sources with photometric quality warnings); $pstar>0.9$ (requires a point-source image profile); $jE1<0.3$, $hE1<0.3$, $k_jE1<0.3$ (limits on ellipticity); $\sqrt{(h_1X_i^2+h_1Eta^2)}<0.3$, $\sqrt{(k_1X_i^2+k_1Eta^2)}<0.3$ (limits on coordinate shifts between passbands).

A further constraint was to limit the search to Galactic longitudes $l>60^\circ$ and $l<358^\circ$. These restrictions were designed to select against blended stellar pairs with inaccurate photometry, which are a frequent occurrence in the most crowded regions of the plane. Only six candidates remained after this procedure. Of these, four were revealed as blended stellar pairs or defective data by inspection of the images and one (a candidate white dwarf) was ruled out by its detection in visible light in the POSS USNO-B1.0 archive. An image of the remaining candidate, UGPS 0722-05, is shown in Fig. 1. The coordinates measured on 2 March 2010 (see §3) were R.A.: $07^h22^m27.29^s$, Dec.: $-05^\circ40^\prime30.0^\prime$. (limits on coordinate shifts between passbands).

## 3 OBSERVATIONS

The Near Infrared Imager and Spectrometer (NIRI) on the Gemini North Telescope on Mauna Kea was used on 10th, 11th and 14th of February 2010 to take spectra covering the $J$, $K$ and $H$ bandpasses respectively, with total on source integration times of 16, 30 and 60 minutes respectively. The spectral resolution was R$\sim$500. They were reduced and calibrated with the IRAF software package using standard tech-
Table 1. Photometry of UGPS 0722-05

| Object       | i   | z   | z   | Y   | J   | H   | K   | [3.6] | [4.5] | L'  | N   | J-H  | H-K |
|--------------|-----|-----|-----|-----|-----|-----|-----|-------|-------|-----|-----|------|-----|
| UGPS 0722-05 | 24.80 | 20.60 | 20.42 | 17.37 | 16.52 | 16.90 | 17.07 | 14.28 | 12.19 | 13.4 | 10.28 | -0.38 | -0.18 |
| Error        | 0.13 | 0.07 | 0.06 | 0.02 | 0.02 | 0.02 | 0.08 | 0.05 | 0.04 | 0.3  | 0.24 | 0.03 | 0.08 |
| Instrument   | GMOS | GMOS | WFC | WFC | WFC | WFC | WFC | IRAC | IRAC | IRCS | T-ReCS |
| Date         | 15/3 | 15/3 | 16/3 | 16/3 | 27/11 | 27/11 | 27/11 | 30/4 | 30/4 | 6/4 | 24/3/13/4 |
| Exposure (s) | 4800 | 120  | 400  | 120  | 80   | 80   | 40   | 1440  | 1440  | 335 | 3360 |

Table 2. Spectral indices for very cool brown dwarfs. Numbers in brackets are the uncertainties on the last 2 digits.

| Object       | W_J  | H2O-J | CH4-J | NH3-H | H2O-H | CH4-H | CH4-K | K/J   |
|--------------|------|-------|-------|-------|-------|-------|-------|-------|
| UGPS 0722-05 | 0.258 | 0.025 | 0.162 | 0.535 | 0.122 | 0.086 | 0.104 | 0.121 |
| T9 average   | 0.1358(19) | 0.4917(21) | 0.1218(17) | 0.0643(13) | 0.0959(22) | 0.12615(33) |
| T8 0415-09   | 0.31  | 0.030 | 0.168 | 0.625 | 0.173 | 0.105 | 0.05  | 0.134 |

4 RESULTS

4.1 Spectroscopy

The near-infrared spectrum of UGPS 0722-05 (Fig. 2, upper panel) is broadly similar to that of a T9 dwarf. However, a ratio plot comparing UGPS 0722-05 with the average of three T9 dwarfs (Fig. 2, middle panel) shows that the broad molecular absorption troughs on either side of the flux peaks at 1.28 µm and 1.59 µm and on the long wavelength side of the 1.07 µm peak are between 10% and 30% deeper. The values of the spectral indices “W_J”, “CH4-J”, “NH3-H” and “CH4-H”, which are used for typing the coolest T dwarfs (see B08) are smaller than those of T9 dwarfs by amounts similar to the differences between T8 and T9 dwarfs, see Table 1. We therefore assign a spectral type of T10. The expanded view of the J band spectrum (Fig. 2, lower panel) shows a narrow absorption feature at 1.275 µm that has an equivalent width of 3.6±0.1 Å. A feature has been seen at a similar wavelength in Jupiter and (weakly) in a T8.5 dwarf and a T9 dwarf (see B08). We have examined a synthetic NH3 spectrum generated from a new high temperature line list (see Yurchenko et al. 2009; Yurchenko et al.,in prep) but there is no sign of a corresponding feature. The only candidate NH3 absorption feature in the spectrum is a weak detection in the H band, at 1.514 µm (not shown). This is the wavelength of the strongest feature produced by a group of lines at 1.4<λ<1.6 µm in the synthetic spectrum, when binned to the same resolution as the data. We caution that no conclusion can be drawn from this comparison until the line list is incorporated into a full model atmosphere.

In Fig. 2 (bottom panel) we overplot a BT-SETTL model atmosphere spectrum (see Allard et al. 2007), computed for effective temperature Teff=500 K, g=10^4 cm s^-2 and [M/H]=0.0. Comparison with the data indicates that some marginally detected narrow absorption features, e.g. at 1.282 µm, are probably real. Most of the narrow absorption features that appear in the model are due to H2O (the NH3 and CH4 lists employed are highly incomplete in the J band). H2O is a possible carrier of the 1.275 µm feature. Another is H2F, which has some absorption lines at wavelengths close to this that are included in the models. This possibility was also suggested by Y.Pavlenko (private comm.). Despite the reasonable qualitative agreement between the model and the data in the J band, the overall 1-2.5 µm SEDs predicted by all the BT-SETTL models at Teff=400-600 K (not shown) are much bluer than we observe.

4.2 Parallax and proper motion

An astrometric analysis was performed using the UKIRT and 2MASS data with a sample of 8 reference stars near UGPS 0722-05, using methods described in Tinney et al. (2003). The chosen stars surround the target, range in brightness from 1.9 mag brighter to 0.1 mag fainter than it (most are within 0.3 mag), and are found in both the 2MASS and UKIRT images. The scatter of the residuals about the astrometric solution for reference stars within ±0.2 mag of UGPS 0722-05 in UKIRT data is 6.2 mas. We adopt this as the astrometric precision for the T dwarf at each epoch.

The astrometric solution for UGPS 0722-05 using the UKIRT data alone clearly shows that it is nearby (see Table 3 – the relative parallax is the weighted mean of those arising from the right ascension and declination solutions). However, the non-optimal sampling of its proper motion results in some concerns about degeneracy impacting on the parallax solution. Fortunately, the 2MASS datum helps us to refine the solution. Even though the observation has low signal-to-noise (the astrometric precision for the reference stars is ~40 times lower than the UKIRT images) it adds in a much longer time baseline to constrain the proper motion. The UKIRT+2MASS solution (shown in Fig.3 for the 2006-2010 period) is consistent with the UKIRT-only solution (see Table 3), giving us confidence that the distance to this object has been well constrained. At d=4.1±0.6 pc UGPS 0722-05 is the closest isolated brown dwarf known.

Two even closer stars with brown dwarf companions are known: c Indi (Scholz et al. 2003) and SCR 1845-6357 (Biller et al. 2006). We note that neither the Gemini acquisition images (with 0.4′′ resolution) nor the Spitzer images reveal any sign of a companion. A proper motion search for companions with the SuperCosmos archive also found nothing.
5 ANALYSIS AND DISCUSSION

UGPS 0722-05 has absolute J band magnitude, M_J = 18.5 ± 0.2, which is fainter than any other brown dwarf. Marocco et al. (in prep.) have measured parallaxes for a large sample of T dwarfs and plotted M_J vs. spectral type. Our assigned spectral type of T10 is consistent with the general trend that they report, within the scatter.

UGPS 0722-05 has H-[4.5] = 4.71, which is redder than any other brown dwarf except the metal poor T7.5p dwarf SDSS J1416+13B (Burningham et al. 2010b). The H-[4.5] colour is considered a good indicator of T_eff (see e.g. L10a) so this supports our inference from the near-infrared spectrum that UGPS 0722-05 is cooler than the three known T9 dwarfs, for which 4.0 ≤ H-[4.5] ≤ 4.5. The i-z, z-Y, Y-J, J-H and H-K colours of the object are similar to those of the T9 dwarfs. While the H-[4.5] colour is considered a good indicator of T_eff, it is also influenced by metallicity and gravity (L10a). Recent estimates of the distance to SDSS 1416+13B (d ≈ 8 pc, see Scholz 2010; Burgasser et al. 2010) indicate that it is more luminous than UGPS 0722-05 by a factor of ~2. Assuming that these estimates are not greatly in error, they indicate that the redder colour of SDSS 1416+13B is due to a combination of low metallicity and high gravity, which would also explain the extremely blue H-K colour (see e.g. Leggett et al. 2009). As Burgasser et al. (2010) pointed out, this implies that the T_eff of SDSS 1416+13B is somewhat higher than the 500 K value that Burningham et al. (2010b) derived from the colours in the absence of a significant luminosity constraint. We therefore conclude that UGPS 0722-05 is the coolest brown dwarf known.

To calculate the total luminosity of the object we summed over the SED as follows. The flux-calibrated near-infrared spectrum covers the range 1.035 < λ < 2.54 μm. For the 0.94-1.035 μm we used the spectrum of the T9 dwarf ULAS J003402.77-005206.7 (hereafter 0034-00, Warren et al. 2007), scaled to the Y magnitude of UGPS 0722-05. The negligible flux at λ < 0.94 μm was not included. For 3.92-4.00 μm we used the spectrum of the T8 dwarf 2MASS J04151954-
0935066 (hereafter 0415-09, Saumon et al. 2007, hereafter S07), scaling to the 3.6 \( \mu \text{m} \) flux. The fluxes in the 3.6 \( \mu \text{m} \) IRAC and T-ReCS \( N \) (7.7-13.0 \( \mu \text{m} \)) passbands were calculated using the flux-calibrated spectra of 0415-09 (S07) and the T9 dwarf ULAS J133553.45+113005.2 (hereafter 1335+11, Leggett et al. 2009) respectively. BT-SETTL models with \( T_{\text{eff}} = 500-600 \text{ K} \) and \( \log(g) = 4.0-5.0 \), [M/H]=0.0 were used for the 4.5 \( \mu \text{m} \) magnitude to flux conversion (lacking a suitable measured spectrum). The same models were used to estimate the flux at \( \lambda > 13.0 \text{ \mu m} \), at 2.54-3.18 \( \mu \text{m} \) and at 5.02-7.70 \( \mu \text{m} \), scaling with the aid of fluxes in adjacent measured passbands. The fluxes in these wavelength intervals have large uncertainties, owing to a strong dependence on model parameters.

The total luminosity of UGPS 0722-05 is \( L = 9.2 \pm 3.1 \times 10^{-7} \text{ } L_{\odot} \), where the uncertainty arises from a 19\% uncertainty in the total flux and the 13\% uncertainty in the distance. This compares with \( L = 1.1 \pm 0.1 \times 10^{-6} \text{ } L_{\odot} \) for the T9 dwarfs 0034-00 and 1335+11 (Marocco et al., in prep) and \( L = 9.8 \pm 0.1 \times 10^{-7} \text{ } L_{\odot} \) for the T8.5 dwarf Wolf 940B (Leggett et al. 2010b), all of which have more fully measured SEDs and much more precise parallaxes.

Assuming an age in the range 0.2-10 Gyr, the evolutionary models of Saumon & Marley (2008, hereafter SM08), allow a radius, \( R \), between 0.085 \( R_{\odot} \) (at 10 Gyr) and 0.12 \( R_{\odot} \) (at 0.2 Gyr). Using the definition of \( T_{\text{eff}} = L/4\pi R^2 \sigma T_{\text{eff}}^4 \), we calculate \( T_{\text{eff}} = 614 \pm 46 \text{ K} \) for \( R = 0.085 \text{ } R_{\odot} \) and \( T_{\text{eff}} = 516 \pm 39 \text{ K} \) for \( R = 0.12 \text{ } R_{\odot} \).

Model atmospheres are not presently considered to be reliable at such low temperatures. Nonetheless, some indication of physical properties can be gained by consideration of evolutionary models and model atmospheres, aided by comparison with other late T dwarfs (see e.g. L10a). UGPS 0722-05 has \( H-K = -0.18 \pm 0.08 \) and \( M_H \lesssim 18.8 \). In the top panel of fig. 9 of L10a it would lie at the bottom of the plot under Wolf 940B, indicating that the dwarf has similar gravity and metallicity to the T9 dwarfs 0034-00 and 1335+11 but is significantly cooler, with \( T_{\text{eff}} \approx 500 \text{ K} \). Exactly the same conclusion can be drawn from placing it in the \( H-K \) vs. \( H-[4.5] \) diagram in fig. 7 of Leggett et al. (2009). The similarity otherwise to the three T8.5 to T9 dwarfs implies that UGPS 0722-05 has solar or slightly enhanced over solar metallicity. Its small tangential velocity (\( \sim 19 \text{ km/s} \)) suggests that it is not a very old object.

The luminosity calculation permits effective temperatures in the range 477-660 K (allowing for the uncertainties in \( L \) and \( R \)). However, similar calculations for the T9 dwarfs 0034-00 and 1335+11 (which have well measured luminosities), find \( T_{\text{eff}} = 530-660 \text{ K} \) for both objects (Marocco et al., in prep) and models indicate \( T_{\text{eff}} \approx 600 \text{ K} \) for 1335+11 (B08, Leggett et al. 2009). The mature age benchmark T8.5 dwarf Wolf940B has \( T_{\text{eff}} \approx 600 \text{ K} \) (Leggett et al. 2010b), which is based on a well measured luminosity and a well constrained radius. Since UGPS 0722-05 is clearly cooler than these three objects, which have bluer \( H-[4.5] \) colours and earlier spectral types, we can be confident that its effective temperature is in the lower half of the range permitted by the luminosity. We adopt \( T_{\text{eff}} = 480-560 \text{ K} \) as the most likely range for this object. This is consistent with the 500 K value indicated by the SM08 models. At 480-560 K, the SM08 models indicate a mass in the range 5 to 15 \( M_{Jup} \), \( \log(g) = 4.0 \) to 4.5 and age of 0.2 to 2.0 Gyr.

Whilst we have provisionally designated it as a T10 dwarf, we note that it is unusual for the range of sub-types to run from 0-9. It is therefore quite possible that UGPS 0722-05 will come to be seen as the first example of a new spectral type. The fairly strong 1.275 \( \mu \text{m} \) feature might perhaps form the basis of such a classification. Gross changes in 1-2.5 \( \mu \text{m} \) spectra are not expected in cooler objects, given the similarity of T dwarf spectra to that of Jupiter (see B08) but the near-infrared component of the SED will decline.

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