Abstract In contrast to the complex nature of slope failures, physically-based slope stability models rely on simplified representations of landslide geometry. Depending on the modelling approach, landslide geometry is reduced to a slope-parallel layer of infinite length and width (e.g., the infinite slope stability model), a concatenation of rigid bodies (e.g., Janbu’s model), or a 3D representation of the slope failure (e.g., Hovland’s model). In this paper, the applicability of four slope stability models is tested at four shallow landslide sites where information on soil material and landslide geometry is available. Soil samples were collected in the field for conducting respective laboratory tests. Landslide geometry was extracted from pre- and post-event digital terrain models derived from airborne laser scanning. Results for fully saturated conditions suggest that a more complex representation of landslide geometry leads to increasingly stable conditions as predicted by the respective models. Using the maximum landslide depth and the median slope angle of the sliding surfaces, the infinite slope stability model correctly predicts slope failures for all test sites. Applying a 2D model for the slope failures, only two test sites are predicted to fail while the two other remain stable. Based on 3D models, none of the slope failures are predicted correctly. The differing results may be explained by the stabilizing effects of cohesion in shallower parts of the landslides. These parts are better represented in models which include a more detailed landslide geometry. Hence, comparing the results of the applied models, the infinite slope stability model generally yields a lower factor of safety due to the overestimation of landslide depth and volume. This simple approach is considered feasible for computing a regional overview of slope stability. For the local scale, more detailed studies including comprehensive material sampling and testing as well as regolith depth measurements are necessary.

Keywords Slope failure · Landslide geometry · Infinite slope stability model · Janbu’s model · r.slope.stability · Differential digital terrain model

Introduction Landslides are a common geomorphological feature in mountain regions often putting lives and infrastructure at risk. The term “shallow landslides” typically refers to translational sliding movements of soil material (earth and/or debris), characterized by a pre-defined, planar sliding surface in a depth of up to 2.0 m (e.g., Cruden and Varnes 1996; Hungr et al. 2014). In the past decades, the Laternser valley (Vorarlberg, Austria) was repeatedly affected by rainfall-triggered shallow landslides (Andrecs et al. 2002; Markart et al. 2007). Since the 1950s, more than 800 shallow landslides have been documented in a comprehensive shallow landslide inventory (Zieher et al. 2016). To be aware of the associated risks, it is necessary to assess shallow landslide susceptibility, hazard, and risk area-wise. Various techniques have been proposed for landslide susceptibility modelling/mapping (i.e., heuristic, statistically-, and physically-based). Amongst them, physically-based landslide susceptibility models employ physical laws to assess slope stability. They typically rely on the limit equilibrium concept relating to destabilizing forces. The proposed techniques differ in the complexity of the considered landslide geometry (shape of the potential sliding surface) in two (e.g., Bishop 1955; Fellenius 1927; Janbu 1954; Morgenstern and Price 1965) and three dimensions (e.g., Hovland 1977; Hungr 1987; Lam and Fredlund 1993; Mergili et al. 2014). While slope failures show complex geometrical shapes in nature, their representation in physically-based slope stability models is simplified. Shallow landslides are approximated by either a slope-parallel layer of infinite length and width (e.g., the infinite slope stability model, ISSM), a concatenation of rigid bodies of infinite width (e.g., Janbu’s model), or a representation of discrete, 3D units (columns on the basis of raster cells; e.g., the r.slope.stability model, RSS). Consequently, the considered sliding surfaces are either planar (ISSM), an irregular 2D polyline (2D models) or an irregular 3D surface (3D models). Furthermore, some of these approaches include inter-slice forces between the geometrical subunits (e.g., Janbu 1954) while others assume them to cancel each other out (e.g., Fellenius 1927). The result of physically-based slope stability models based on the limit equilibrium concept is a dimensionless factor of safety (FOS) which is a quantitative measure of slope stability. Slope failures are predicted, if the FOS falls below 1. In engineering, these models are usually applied at local scale to evaluate the stability of a single slope unit in the context of a specific engineering task. For the assessment of slope stability at catchment scale, the ISSM has proven feasible in combination with geographical information systems (GIS). Most spatially distributed physically-based shallow landslide susceptibility models include the infinite slope approach, often combined with an infiltration model (e.g., Baum et al. 2008; Dietrich et al. 1995). Recently, models including a more complex landslide geometry (e.g., ellipsoidal and truncated sliding surfaces) have been implemented in GIS (Mergili et al. 2014; Xie et al. 2006). For all these physically-based slope stability models, the result is a FOS map which is a spatially distributed quantitative measure of slope stability.

Besides geotechnical input parameters characterizing the involved material, physically-based models require data on topography (e.g., slope angle) and depth of the pre-defined sliding surface. Topographic data are usually derived from digital terrain models (DTMs), which have become readily available. The depth of the pre-defined sliding surface is more difficult to obtain. It can be assessed by (i) direct measurements (Andrecs et al. 2002; Wiegand et al. 2013), (ii) means of geophysics (Davis and Annan 1989; Sass 2007), or modelling (Dietrich et al. 1995; Catani et al. 2010). Moreover, depth and volume of past landslides can be...
assessed efficiently with the help of multi-temporal remotely sensed elevation data (Zieher et al. 2016).

Numerous studies have focussed on the area-wide assessment of slope stability at catchment scale by applying physically-based slope stability models which include the infinite slope approach (e.g., Baum et al. 2005; Gioia et al. 2016; Montrasio et al. 2011). In such studies, little attention has been paid to the effect of the simplified landslide geometry considered by the ISSM. However, this issue must be regarded for the interpretation of the resulting FOS maps. In this paper, four slope stability models including different representations of landslide geometry are tested at four sites affected by shallow landslides, where information on soil material properties and geometries of slope failures are available. Simplifications of the models with regard to landslide geometry are tested against real-world geometries of the selected cases. The applicability of the widely used infinite slope stability model is investigated in detail. The ISSM’s predictions are compared to the results of models with 2D (Janbu’s model) and 3D (r.slope.stability, 3DV A) approximations of the slope failures. For the comparison of the methods, models with comparable physical basis but different geometrical representations of the slope failures were chosen. Further influencing factors such as effects of high vegetation (root cohesion) or variable soil saturation were neglected. Omitting the root cohesion together with the assumption of completely saturated conditions is considered as worst-case scenarios. Under equal conditions for the applied models, the results are better comparable.

The objectives are as follows:

1. To conclude on the ability of the tested models to reproduce the observed landslides with the given parameterization;
2. To learn about the effects of different representations of landslide geometry on the respective model results;
3. On this basis, to identify potential pitfalls in slope stability modelling.

The present article is divided into four main sections. First, the study area including the landslide-triggering rainfall event in August 2005 is described in the “Study area” section. The conducted laboratory experiments, the landslide geometry data, and the modelling approaches are introduced in the “Materials and methods” section. Model results and comparisons are presented and discussed in the “Results and discussion” section. Finally, concluding remarks summarizing the key findings are provided in the “Conclusions” section.

Study area
The four test sites are located in the Laternser valley in Vorarlberg, Austria (Fig. 1). This valley, extending about 13 km in the East-West direction, follows the general strike angle of the Bregenzerwald Mountains. The four sampled landslide locations are situated on the south-facing hillside in the vicinity of the valley’s main settlements (Fig. 1). Abbreviations are given according to the closest settlements (BIN Bingadels, BON Bonacker, MAZ Mazona, ROH Rohnen). All four shallow landslides were triggered in the course of a rainfall event on 22/23 August 2005. The landslides at the locations BIN, BON, and ROH were also mapped by (Markart et al. 2007) immediately after the event. Table 1 shows the metadata for the four landslide sites.

Tectonics and geology
The tectonic structure of the valley is dominated by various nappes. Helvetic nappes in the western and northern part of the valley are characterized by competent limestones (e.g., Schrattenkalk, Seeuvkalk) and marls with calcareous layers (e.g., Drusbergschichten). Superimposed to the south-east, ultrahelvetic nappes are mostly built up of clayey marls and shales (e.g., Leinermurmel). On top extending to the south-east, penninic nappes underlie more than half of the valley. These are characterized by sandstones (e.g., Reiselsberger Sandstein, Plankerbrückenserie) and thinly layered marls (e.g., Piesenkopfschichten) (Friebe 2007; Heissel et al. 1967; Oberhauser 1982; Oberhauser 1998). Above all, the widespread moraine deposits as well as hillside debris are overly susceptible to shallow landsliding. In many cases, subglacial till is reported to form an impermeable layer acting as a sliding surface for the unconsolidated material on top. Only in rare cases also subglacial till was mobilized. Additionally, marls of the Ultrahelveticum, often forming dip slopes, and less competent sandstones of the Penninicum are overly affected by shallow landslides (Zieher et al. 2016).

Climate
Due to the influence of oceanic air masses, the climate of Vorarlberg is generally more balanced compared to the whole of Austria. Generally, precipitation amounts are higher on the fringe of the Alps in northern Vorarlberg due to blockage effects of the inflowing air masses (Werner and Auer 2001a; Werner and Auer 2001b). The Laternser valley opens up to the west and is therefore prone to north and north-westerly weather conditions. At Innerlaterns station (location mapped in Fig. 2), the mean annual precipitation exceeds 1700 mm. In the study area, exceptional amounts of rainfall have been identified as the main trigger of shallow landslides (Andrecs et al. 2002; Markart et al. 2007).

Landslide-triggering rainfall event on 22/23 August 2005
Antecedent rainfall conditions from November 2004 on to the 22/23 August 2005 event generally fell below the long-term mean. Therefore, it can be expected that the antecedent soil moisture preceding the rainfall event was below average. Effects of snow can be excluded during the summer months. After days with minor rainfalls in mid-August, a phase of intense precipitation started on August 22. At Innerlaterns station, the cumulative precipitation sum of the rainfall event amounted to 256 mm (Fig. 2a). The highest rainfall intensity was recorded in the late evening on August 22 and during the night hours (21 to 22 p.m. 19.4 mm/h). With the help of multiple orthophoto series and two DTMs based on airborne laser scanning (ALS), a detailed shallow landslide inventory was prepared (Zieher et al. 2016; Fig. 2b). In total, 478 shallow landslides associated with the rainfall event in August 2005 were mapped.

Materials and methods
Test sites and field work
Geotechnical samples were collected at four sites where shallow landslides had been triggered in the course of the rainfall event in August 2005. The slope failures occurred during the night hours from 22/23 August. Therefore, hardly any eyewitness reports on
the exact time of failure are available throughout the valley. In the geological map (Fig. 1b), the sampled shallow landslide locations are mapped as hillslope debris (BIN), till deposits (BON, MAZ), and Drusbergschichten (marls with calcareous layers; ROH). These geological units have been identified as overly susceptible to shallow landsliding in the Laternser valley (Zieher et al. 2016). Particularly, the slope-parallel dipping marls of the Amdener Mergel (BIN), Leimernmergel (BON, MAZ), and Drusbergschichten (ROH) provide potential sliding surfaces at the bedrock-regolith interface. Stabilizing effects of high vegetation can be excluded at the test sites BON and MAZ as these landslides occurred on extensively used grass land. In case of the slope failures at the test sites BIN and ROH, single trees above the scarp may have contributed to the stability of the slopes. The four landslides turned into debris avalanches (BIN, BON, MAZ) and a debris flow (ROH) with runout distances of up to 150 m. Accumulated material on roads and within agricultural areas was removed subsequently.

Back walls were laid open at the scarp of the shallow landslides. The sampling strategy comprised two undisturbed and one disturbed sample at two depths at each site. At one site (ROH), samples at one depth were considered sufficient due to the homogeneous structure of the regolith. Undisturbed samples were taken with a core cutter and stored airtight. In addition, one bucket of material was sampled at the respective depths. Samples obtained

![Fig. 1 Location of the Laternser valley and its geological substratum. Only geological units covering more than 1% of the valley are listed in the legend (modified after Zieher et al. 2016). Sampled landslide locations are mapped as dots](image)

### Table 1 Metadata for the four sampled landslide sites and results of the conducted laboratory tests

| Parameters                      | BIN      | BON      | MAZ      | ROH      |
|---------------------------------|----------|----------|----------|----------|
| Latitude (degree)               | 47.2722  | 47.2673  | 47.2679  | 47.2699  |
| Longitude (degree)              | 9.7040   | 9.7256   | 9.7352   | 9.7001   |
| Scar area (m²)                  | 437      | 363      | 1036     | 487      |
| Sample depth 1 (cm)             | 45       | 30       | 37       | –        |
| Sample depth 2 (cm)             | 92       | 80       | 67       | 108      |
| Depth of landslide crown (m)    | 1.1      | 1.2      | 0.9      | 1.7      |
| Angle of internal friction (degree) | 25.9    | 30.3     | 29.3     | 37.2     |
| Cohesion (kPa)                  | 5.6      | 6.2      | 4.6      | 17.6     |
| Plastic limit (mass %)          | 23.5     | 26.8     | 26.6     | 18.9     |
| Liquid limit (mass %)           | 40.0     | 46.2     | 41.8     | 23.1     |
| Dry density (g/cm³)             | 1.36     | 1.37     | 1.45     | 1.99     |
| Porosity (%)                    | 46.3     | 48.9     | 45.1     | 25.5     |
| Soil type                       | Clay; medium plastic | Clay; medium plastic | Silt; medium plastic | Clay/silt; slightly plastic |

2011 Landslides 14 • 2017
in the upper part of the back wall were used for the derivation of hydrological properties mainly. Lower samples were used for the estimation of geotechnical parameters (angle of internal friction, cohesion, Atterberg limits). Water contents, wet and dry bulk densities, as well as grain size distributions were determined for all samples. Figure 3 shows the grain size distributions and the Atterberg limits for the tested samples.

At test site BON, the regolith depth above the landslide scarp was assessed by dynamic cone penetration tests (DCPTs, locations mapped in Fig. 4). A lightweight dynamic cone penetrometer including a rammer of 10 kg dropped from a height of 0.5 m was used (e.g., Wiegand et al. 2013; Perumpral 1987). In accordance with (ÖNORM EN ISO 22476-2:2012 2012), the necessary number of strokes to penetrate through increments of 10 cm was recorded. If the vertical increment after completing 50 strokes was less than 10 cm, the penetration tests were stopped (ÖNORM EN ISO 22476-2:2012 2012). The locations of the DCPTs were measured using a differential global positioning system (dGPS).

For the study area, high-resolution DTMs of two ALS campaigns in 2004 (1.0 m cell size) and 2011 (0.5 m cell size) are available area-wide. The subtraction of both DTMs (differential digital terrain model; dDTM) yields the height difference between the times of acquisition. Shallow landslide scar areas are detectable as distinct features characterized by a decrease in elevation, i.e., a loss of volume (Fig. 4). Table 2 shows the reported point densities and accuracies of the two ALS campaigns conducted area-wide for the state of Vorarlberg. These numbers are minimum requirements which must be provided throughout the scanned area. Therefore, the acquired point density is typically higher. At the test sites, the actual point density for 2004 is between 1.9 and 5.0 pts m$^{-2}$ while it is distinctively higher for 2011 with 15.4–19.5 pts m$^{-2}$. Also the error margins, including systematic errors, positional uncertainty due to the size of the laser beams’ footprints, and the registration error, must be

![Fig. 2](image-url) Hourly and cumulative precipitation time series (Innerlaterns station) of the landslide-triggering rainfall event on 22/23 August 2005 as well as the inventory showing all mapped shallow landslides for this event (b). The location of Innerlaterns station is shown in b.

![Fig. 3](image-url) Resulting grain size distributions (a) and Atterberg limits (b) for the tested samples.
provided area-wide and are hence conservative. In addition, none of the scar areas at the test sites re-vegetated. Particularly, low vegetation would have an adverse impact on the positional accuracy. It has been therefore generally assumed that (i) the accuracies of the ALS point clouds are sufficient for accurately detecting landslide depths for the purpose of the present study and (ii) the morphology of the landslide scars is sufficiently represented by the derived raster datasets. In addition, it is presumed that the surface mainly changed due to shallow landsliding and further processes play a minor role.

Within the scar area, the dDTM gives an estimate of the vertical landslide depth (Fig. 5). Two landslides are rather shallow (BIN, BON) extending to a depth of 1.6 m while the other two are generally deeper (MAZ, ROH) with up to 3.3 and 4.5 m, respectively. Regarding the type of movement, depth-to-length ratios are frequently used to differentiate between translational and rotational landslides (e.g., Cruden and Varnes 1996; Skempton and Hutchinson 1969). Translational landslides are characterized by a low depth-to-length ratio of typically less than 0.1 (Cruden and Varnes 1996). Based on this criterion, all four landslides are of the translational type (Table 3).

Slope angles derived from the first DTM provide estimates of the inclination of the original surface before the landslides occurred. The evaluation within the scar areas results in slope angle distributions (Fig. 6). Theoretically, slope angles within the scar areas derived from the second DTM show the inclination of the sliding surface. For the landslide locations BIN and BON, no significant changes of median and mean slope angles are noticeable while their variance increased. This can be attributed to the side walls of the landslides biasing the slope angle values within the scar area. For the landslide location MAZ, a slight increase and for location ROH, a slight decrease of median slope angles is evident. Compared to the pre-event surface, this could indicate a steeper sliding surface at test site MAZ and a less inclined sliding surface at test site ROH. However, these distributions show possible value ranges for the slope angle as input parameter for the ISSM. The slope angle distributions were calculated based on the tangent and are shown in degrees. Table 4 shows statistics of the slope angle distributions evaluated within the scar areas.

Figure 7 shows the real-world geometry of the four shallow landslides represented in the dDTM and principles of the landslide geometry considered in the three types of models. The ISSM and

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**Table 2** Metadata of the two ALS campaigns covering the state of Vorarlberg

| ALS campaign | Point density demanded | Reported accuracy | Vertical | Spatial resolution |
|--------------|------------------------|-------------------|----------|-------------------|
| 2004         | 1 pt per m²            | –                 | ±20 cm   | 1.0 m             |
| 2011         | 4 pts per m²          | ±10 cm            | ±7.5 cm  | 0.5 m             |

*In 2011, a minimum point density of 8 pts per m² is provided in the vicinity of main rivers*
Janbu’s model are based on simplified approximations of the geometry. Only the 3D approaches include the details of locally varying landslide depth also in lateral direction.

Infinite slope stability model

The ISSM relies on a limit equilibrium approach relating stabilizing to destabilizing forces (Fig. 8). In the model, the landslide geometry is reduced to a slope-parallel layer of infinite length and width on top of an inclined, slope-parallel sliding surface (Fig. 7e). Assuming fully saturated conditions and slope-parallel ground water flow, the FOS is calculated from:

$$FOS = \frac{T}{S} = \frac{c' \cdot l + N' \cdot \tan \phi'}{W \cdot \sin \beta + F_s}$$

where \(c'\) is the effective cohesion, \(l\) is the unit length, \(N'\) is the effective normal force, \(\phi'\) is the effective angle of internal friction of the soil material, \(W\) is the effective weight of saturated soil, \(\beta\) is the slope angle, and \(F_s\) is the seepage force. All forces are calculated as unit forces where the width corresponds to 1 unit length (e.g., Mergili et al. 2014; Fellin 2014; Ghiassian and Gharab 2008). The model’s formulae and the workflow for parameter testing were implemented in the R open source software environment for statistical computing (R Core Team 2016).

The results of the ISSM are highly sensitive to the parameters representing landslide geometry assumed by the model (i.e., slope angle and landslide depth). The model was applied for the four sampled landslide locations assuming the results of the laboratory tests to be representative for the local material characteristics. Based on the respective parameter values (i.e., specific weight, effective cohesion, and effective angle of internal friction; Table 1), the impact of landslide depth and slope angle is assessed in detail.

Janbu’s model

The model after (Janbu 1954) follows the limit equilibrium concept and is based on polygonal sliding surfaces with longitudinal slices of defined lateral length and infinite width (Fig. 9). For the limit equilibrium, all forces acting on each single slice in its center of mass are taken into account. Compared to the ISSM, a more complex 2D geometry of the sliding surface can be reproduced (Fig. 7f). The landslide geometries of the four test sites were obtained from the available pre- and post-event DTM’s along slope-parallel profiles (Fig. 10). The FOS was calculated using the software GGU-Stability (GGU 2016) employing the following formula:

$$FOS = \frac{\sum(T_i + E_i)}{\sum(S_i + E_{i+1})} = \frac{\sum(c' \cdot l_i + N'_i \cdot \tan \phi' + E_i)}{\sum(W'_i \cdot \sin \beta_i + F_s + E_{i+1})}$$

where the sum of resisting forces \(T_i\) and stabilizing forces from adjacent slices \(E_i\) are related to the sum of driving forces \(S_i\) and destabilizing forces from adjacent slices \(E_{i+1}\) for each slice \(i\). All forces are calculated as unit forces where the width corresponds to 1 unit length. \(c'\) is the effective cohesion, \(l_i\) is the length of slice \(i\), \(N'_i\) is the effective normal force, \(\phi'\) is the effective angle of internal friction.
friction, $E_i$ is a stabilizing force resulting from the passive earth pressure exerted by the slice below, $W'_i$ is the slice’s weight of saturated soil, $F_{s_i}$ is the seepage force, and $E_{i+1}$ is a destabilizing force resulting from the active earth pressure exerted by the slice above.

### 3D approaches

The r.slope.stability model (Mergili et al. 2014) evaluates the slope stability conditions for one to many randomly selected ellipsoidal sliding surfaces. By default, the longest half axis is aligned along the steepest slope. The ellipsoids can be truncated in order to consider irregular sliding surfaces such as the bottom of soil, shallow weak layers, or shallow discontinuities bounded by hard bedrock. To compute the FOS, r.slope.stability employs a modified version of the 3D sliding surface model of (Hovland 1977), revised and extended by (Xie et al. 2006; Xie et al. 2003; Xie et al. 2004a; Xie et al. 2004b):

$$FOS = \frac{\sum_i T_i}{\sum_i S_i} = \frac{\sum_i (c' \cdot a_i + (W'_i \cdot \cos \beta_{zi} + N_i) \cdot \tan \phi') \cdot \cos \beta_{m_i}}{\sum_i (W'_i \cdot \sin \beta_{zi} + F_{s_i}) \cdot \cos \beta_{m_i}}$$  

(3)

where $a_i$ is the basal area of each soil column derived from

$$a_i = s_r^2 \sqrt{1 - \left(\sin^2 \beta_{xz_i} \cdot \sin^2 \beta_{yz_i}\right) / \cos \beta_{xz_i} \cdot \cos \beta_{yz_i}}$$  

(4)

where $s_r$ is the cell size for squared raster cells, $\beta_{xz_i}$ is the slope angle component in east-west direction, and $\beta_{yz_i}$ is the slope angle component in north-south direction (Xie et al. 2003). In Eq. 3, resisting forces $T$ and driving forces $S$ are summed over all columns $i$ within the scar area. $c'$ is the effective cohesion per unit area, $W'_i$ is the effective weight of saturated soil, $\beta_{zi}$ is the inclination of the sliding surface at the considered column, $\phi'$ is the effective angle of internal friction, and $\beta_{m_i}$ is the apparent dip of the sliding surface at the considered column in downslope direction (alignment of the ellipsoid). $N_i$ and $F_{s_i}$ are the contributions of the seepage force to the normal force and the shear force. No inter-column forces are considered. The principles of the FOS calculation are discussed in detail by (Mergili et al. 2014). r.slope.stability further includes several functionalities to combine the FOS values computed for various sliding surfaces to landslide susceptibility maps (Mergili et al. 2014). In the present work, however, single truncated sliding surfaces are used, corresponding to the sliding surfaces of the considered shallow landslides.

A simplified 3D volumetric approach (3DVA) is based on discrete soil columns represented in a raster environment assuming slope-parallel ground water flow (Fig. 11). In contrast to r.slope.stability, considering a main direction of the slope failure for the calculation of driving and resisting forces, all forces are calculated for each column based on its inclination and aspect. The FOS is the ratio of the sums of resisting forces $T_i$ and driving forces $S_i$ for all columns $i$ within the scar area:

$$FOS = \frac{\sum_i T_i}{\sum_i S_i} = \frac{\sum_i (c' \cdot a_i + N_i \cdot \tan \phi')}{\sum_i (W'_i \cdot \sin \beta_{zi} + F_{s_i})}$$  

(5)

where $c'$ is the effective cohesion per unit area and $a_i$ is the basal area of each soil column derived from Eq. 4. The slope angle components $\beta_{xz_i}$ and $\beta_{yz_i}$ were computed after (Horn 1981). The effective weight of saturated soil $W'_i$ and the effective normal force are calculated based on each column’s volume. $\phi'$ is the effective angle of internal friction, $\beta_{zi}$ is the inclination of the sliding surface at the considered column, and $F_{s_i}$ is the seepage force. Effects of active and passive earth pressure are neglected.

### Results and discussion

Table 5 shows the resulting values of the FOS for the test sites based on the four tested slope stability models assuming dry and
fully saturated conditions. For the calculations using the ISSM, the median and maximum landslide depths were considered. Assuming dry conditions, all test sites are predicted to be stable by all models. Resulting values for the FOS are well above 1.0 ranging from 1.35 (ISSM; ROH) to 3.48 (r.slope.stability; BON). Considering fully saturated conditions, all test sites are predicted to fail by the ISSM using maximum landslide depths while only at test site MAZ the FOS falls below 1.0 using median landslide depths. Based on Janbu’s model, two slopes would fail and no slope failures are predicted by the 3D approaches. The resulting values for the FOS are between 0.78 (ISSM; MAZ) and 2.15 (RSS; BON). Based on median landslide depths, all test sites except MAZ remain stable. In the following, the results for each modelling approach are described in detail.

Modelling results using the ISSM

Simulations based on median landslide depths result in more stable conditions predicted by the ISSM than for maximum landslide depths. The FOS for dry conditions using the ISSM based on median landslide depths in decreasing order is 2.70 (BON), 2.07 (ROH), 2.01 (BIN), and 1.72 (MAZ), compared to 1.76 (BON), 1.54 (BIN), 1.49 (MAZ), and 1.35 (ROH) for simulations with maximum landslide depths. Assuming fully saturated conditions, all test sites are predicted to fail by the ISSM using maximum landslide depths. Based on median depths, all test sites except MAZ remain stable. The FOS for fully saturated conditions using the ISSM based on medium landslide depths in decreasing order is 1.69 (BON), 1.52 (ROH), 1.23 (BIN), and 0.96 (MAZ), compared to 0.99 (BON), 0.88 (ROH), 0.88 (BIN), and 0.78 (MAZ) for simulations with

Table 4 Statistics of the slope angle distributions evaluated within the scar areas of the four shallow landslides for the two DTM

| Slope angle (degree) | BIN | DTM 2004 | DTM 2011 | BON | DTM 2004 | DTM 2011 | MAZ | DTM 2004 | DTM 2011 | ROH | DTM 2004 | DTM 2011 |
|---------------------|-----|----------|----------|-----|----------|----------|-----|----------|----------|-----|----------|----------|
| Minimum             | 11.3| 3.2      | 3.7      | 4.8 | 8.9      | 4.8      | 9.9 | 22.0      | 2.0      |
| First decile        | 18.5| 14.9     | 10.1     | 9.5 | 17.4     | 17.4     | 31.9| 32.5      | 22.0      |
| First quartile      | 23.1| 21.0     | 21.3     | 17.5| 19.0     | 20.0     | 35.4| 35.6      | 32.5      |
| Median              | 27.4| 27.7     | 27.3     | 28.2| 21.1     | 24.4     | 40.7| 38.8      | 35.6      |
| Mean                | 26.7| 27.9     | 26.7     | 27.5| 22.0     | 24.4     | 39.7| 41.5      | 38.8      |
| Third quartile      | 30.2| 33.3     | 32.2     | 35.0| 24.0     | 27.7     | 43.2| 44.9      | 41.5      |
| Ninth decile        | 32.8| 38.8     | 37.0     | 39.3| 27.7     | 29.6     | 46.3| 50.9      | 44.9      |
| Maximum             | 39.9| 48.5     | 46.3     | 51.0| 38.5     | 44.0     | 52.0| 64.7      | 50.9      |

Statistics are based on tangent and shown in degrees
maximum landslide depths. The ratios between FOS values based on median depths for dry and fully saturated conditions are 1.63 (BIN), 1.60 (BON), 1.79 (MAZ), and 1.36 (ROH). The respective ratios using the maximum landslide depths are 1.75 (BIN), 1.78 (BON), 1.91 (MAZ), and 1.54 (ROH). The latter are higher due to the effects of cohesion. At shallower depths, the stabilizing effect of cohesion is markedly higher than further below (see the “Conclusions” section).

Modelling results using 3D approaches
Both 3D models predict stable slopes at all four test sites for dry and fully saturated conditions. For dry conditions, the FOS values based on the 3DVA in decreasing order are 3.08 (BON), 2.30 (BIN), 2.22 (ROH), and 1.85 (MAZ). Assuming fully saturated conditions, the slopes at the test sites MAZ and ROH are predicted to fail while test sites BIN and BON remain stable. The resulting FOS values in decreasing order are 1.38 (BON), 1.67 (ROH), 1.44 (BIN), and 1.04 (MAZ). Except for location ROH (1.60), the FOS based on RSS is higher with 2.15 (BON), 1.71 (MAZ) compared to that of the 3DVA. The maximum ratios of the FOS assuming dry conditions for each test site between the results of the ISSM for maximum depth and the respective 3D approach are 1.74 (BIN; FOS$_{3DVA}$/FOS$_{ISSM}$), 1.98 (BON; FOS$_{RSS}$/FOS$_{ISSM}$), 2.05 (MAZ; FOS$_{RSS}$/FOS$_{ISSM}$), and 1.64 (ROH; FOS$_{3DVA}$/FOS$_{ISSM}$). Assuming fully saturated conditions, respective FOS values for the 3DVA in decreasing order are 1.95 (BIN), 1.67 (ROH), 1.44 (BIN), and 1.04 (MAZ). Except for location ROH (1.60), the FOS based on RSS is higher with 2.15 (BON), 1.71 (MAZ) compared to that of the 3DVA. The maximum ratios of the FOS assuming fully saturated conditions for each test site between the results of the ISSM for maximum depth and the respective 3D approach are 1.85 (BIN; FOS$_{3DVA}$/FOS$_{ISSM}$),
2.17 (BON; FOS\textsubscript{RSS}/FOS\textsubscript{ISSM}), 2.19 (MAZ; FOS\textsubscript{RSS}/FOS\textsubscript{ISSM}), and 1.90 (ROH; FOS\textsubscript{3DVA}/FOS\textsubscript{ISSM}). Hence, compared to the ISSM, slope stability (the FOS) is overestimated by the 3D models by a factor of around 2.

**Comparison of the results obtained with the various models**

Considering maximum landslide depth, the ISSM yields generally lower FOS compared to the 2D and 3D approaches for either dry or fully saturated conditions. Still, all four test sites were predicted correctly only by the ISSM. Calculations based on the maximum landslide depth indicate stable slopes under dry conditions and slope failures under fully saturated conditions. However, using the maximum landslide depth, the ISSM’s simplified landslide geometry leads to a general overestimation of landslide depth. Hence, also, landslide volumes are overestimated.

Using Janbu’s model, two of four test sites are predicted correctly. At test sites MAZ and ROH, slope failures are predicted assuming fully saturated while slopes at test sites BIN and BON are predicted to remain stable. Compared to the results of the ISSM, the FOS is generally higher. Only in case of test site ROH, the resulting FOS for fully saturated conditions based on Janbu’s model is slightly lower than the corresponding FOS calculated with the ISSM.

Except for location MAZ, the resulting FOS using the 3DVA is distinctively higher than FOS values based on the ISSM or Janbu’s model assuming dry conditions. The FOS using RSS is higher than resulting FOS based on the 3DVA except for location ROH. Resulting FOS values for both 3D approaches are higher than FOS values based on the ISSM and Janbu’s model assuming fully saturated conditions. Although landslide geometry is represented

\[
\begin{align*}
d_i & \quad \text{Regolith depth [m]} \\
a_i & \quad \text{Basal area [m}^2\text{]} \\
s_c & \quad \text{Cell size (square cells) [m]} \\
\beta_i & \quad \text{Slope angle [deg]} \\
\omega_i & \quad \text{Aspect [deg]} \\
\rho_d & \quad \text{Density of dry soil [kg/m}^3\text{]} \\
W_r & \quad \text{Weight of saturated soil [N]} \\
W_e & \quad \text{Effective weight of sat. soil [N]} \\
N & \quad \text{Effective normal force [N]} \\
S & \quad \text{Driving force [N]} \\
T & \quad \text{Resisting force [N]} \\
F_s & \quad \text{Buoyancy [N]} \\
F_v & \quad \text{Seepage force [N]} \\
U & \quad \text{Force due to pore water [N]} \\
\eta & \quad \text{Porosity} \\
g & \quad \text{Acceleration of gravity (9.80665 m/s}^2\text{)} \\
\gamma_d & \quad \text{Unit weight of dry soil [N/m}^3\text{]} \\
\gamma_w & \quad \text{Unit weight of water (9806.65 N/m}^3\text{)} \\
\end{align*}
\]

**Fig. 10** Landslide profiles for calculations with Janbu’s approach at the four test sites (a BIN, b BON, c MAZ, d ROH). The considered slope failures represented by the difference of the two DTM’s are shown in grey.

**Fig. 11** Principle sketch of the 3D slope stability model for fully saturated conditions.
most accurately by the 3D models, both fail to predict any slope failure correctly with the applied parameterization. A possible reason for the inability of the 2D and 3D models to predict the slope failures is the influence of the cohesion in the shallow parts of the landslides. The impact of the cohesion on the resulting FOS decreases non-linearly with depth. Deeper parts of the landslides are predicted to fail with FOS < 1 when considering single pixels, but the whole landslides are predicted to be stable. Including the shallower parts of the landslides in the calculation will enhance the overall FOS (Fig. 12).

In addition, geotechnical parameter values may have been overestimated. For an appropriate determination of the shear parameters, it is important to conduct the shear tests at in situ stress levels. The shear tests have been conducted at the lowest stress levels technically possible (50 kPa). Nevertheless, the in situ stress level of shallow landslides might lie beyond this level (0–40 kPa). This may lead to an overestimation of the cohesion and a slight underestimation of the angle of internal friction for very shallow landslides. Furthermore, single parameter values cannot reflect the local variability of involved material properties.

### Effects of landslide geometry parameters in the ISSM

Effects of the representation of landslide geometry in the ISSM on the resulting FOS are tested in more detail. Principal sketches describing the effects of landslide depth and slope angle on the FOS are shown in Fig. 13. The cumulative distribution of landslide depths shows the proportion of the landslide scar related to a certain depth (e.g., 20% are deeper than 2.3 m). The cumulative slope angle distribution shows the proportion of the landslide scar related to a certain slope angle (e.g., 60% are steeper than 18°). If stability analyses include a cohesion force, the FOS generally decreases non-linearly with depth (Fig. 14). Assuming fully saturated conditions and spatially constant material parameters, the depth of failure can be assessed (FOS falls below 1.0) for various slope angles. Figure 14 shows the FOS as a function of depth for a range of landslide depth values evaluated within the scar areas (Table 4). The depth of failure is compared to the cumulative distribution of landslide depths derived from the dDTM. At least a portion of each shallow landslide is deep enough to fall below a FOS of 1.0 considering the median slope angle (BIN 8.5%, BON 0.3%, MAZ 56.6%, ROH 10.9%). The affected parts are shown in the respective shaded relief. In case of the test sites MAZ and ROH, the area falling below a FOS of 1.0 based on the median slope angle is well connected within the scar area. On the contrary, at test site BIN, the respective area is fragmented and distributed over the scar area.

In the same sense, the FOS decreases non-linearly with increasing slope angle (Fig. 15). Based on a range of landslide depth values evaluated within the scar area (Table 3), the critical slope angle for slope failure (FOS falls below 1.0) is derived and compared to the cumulative distribution of slope angles. The affected areas per depth are shown in the respective shaded relief. Parts of the suspected sliding surface of the locations BIN and MAZ are steep enough for the landslide to fail at median depth (BIN 13.7%, MAZ 57.6%). At the location ROH, 20.4% and 54.1% of the scar area are sufficiently inclined to fail at the third quartile and at the ninth decile of landslide depth, respectively. At the location BON, 1.9% and 30.2% of the scar area are sufficiently inclined to fail at the third quartile and at the ninth decile of landslide depth.

| Site | FOS (dry) | Maximum depth | FOS (saturated) | Maximum depth |
|------|-----------|---------------|----------------|---------------|
| BIN  | 2.01      | 2.68          | 1.81           | 2.30          |
| BON  | 2.70      | 3.08          | 1.90           | 3.15          |
| MAZ  | 1.72      | 1.85          | 1.49           | 1.90          |
| ROH  | 2.07      | 2.22          | 1.35           | 1.55          |

For the ISSM, results for the median and maximum landslide depth using the median slope angle are shown. For the Janbu’s approach and the tested 3D approaches, the results for the median and maximum landslide depth using the median slope angle are shown.

**Table 5**: FOS for the four test sites based on the ISSM, the Janbu’s approach, and the tested 3D approaches for fully saturated and dry conditions (values below 1.0, indicating predicted slope failures, are highlighted).
respectively. However, the side walls of the landslides are generally steeper and should not be considered a potential sliding surface. The ISSM predicts slope failures for parts of all sampled landslide locations. However, according to the ISSM, the location BON almost remains stable even under fully saturated conditions. The parameters representing the landslide geometry in the model could lead to an overestimation of slope stability. The slope angle distribution is known from the DTMs and is considered representative. In Fig. 16b, the penetration resistance and the regolith depth resulting from the DCPTs are compared with the landslide depth derived from the dDTM. Assuming that the underlying Leimernmergel had been reached, regolith depth ranges from 1.5 to 2.7 m in the vicinity of the landslide. Below 1.5 m, the penetration resistance increases markedly. This could indicate an overconsolidated layer or a blocky matrix. The maximum landslide depth of 1.65 m derived from the dDTM within the scar area coincides with the depth below which penetration resistance increases. Hence, the sliding surface may be located on top of this overconsolidated layer. However, it cannot be completely ruled out that the landslide was originally deeper and hence would yield a lower FOS using the ISSM.

Conclusions
In the present study, four physically-based models including different representations of landslide geometry were tested to back calculate real-world slope failures. For the ISSM, the determining parameters for landslide geometry (i.e., slope angle and vertical landslide depth) were tested over ranges derived from DTMs.
Fig. 14 FOS calculated for a range of landslide depths based on various slope angle values (Table 4) for the four landslide locations (a BIN, b BON, c MAZ, d ROH)

Fig. 15 FOS calculated for a range of slope angle values based on various landslide depths (Table 3) for the four landslide locations (a BIN, b BON, c MAZ, d ROH)
within the scar areas. Material parameters were derived from laboratory tests conducted with material samples collected at the four test sites. The model results for the test sites using four approaches were compared. Landslide depths based on the dDTM were validated at one test site with the help of DCPTs.

It is possible to predict the four slope failures using the ISSM. For dry conditions, all test sites remain stable. Assuming fully saturated conditions and representativeness of the geotechnical parameters, the slope failures are predicted (FOS < 1) using the median slope angle derived from the post-event DTM and the maximum vertical landslide depth derived from a dDTM. Using Janbu’s model including a 2D representation of landslide geometry, two out of four failures were predicted for fully saturated conditions. No slope failures were predicted using 3D models. The differing results may be explained by the influence of cohesion.

It is shown that with increasing depth, the influence of cohesion on the FOS decreases non-linearly. Therefore, a more detailed representation of landslide geometry including shallower areas may lead to a higher FOS due to the influence of cohesion. There, the increased stabilizing effect of cohesion enhances the overall FOS. This may explain the higher FOS resulting from the 2D approach (where the shallower parts along the down-slope profile are considered) and the even higher FOS resulting from the 3D approaches (where also the shallower lateral portions of the landslides are considered). The resulting FOS based on the ISSM using the median landslide depth better corresponds to the results of the 2D and 3D approaches.

Field measurements theoretically yield the maximum regolith depth. If the bedrock acts as the sliding surface, the maximum regolith depth corresponds to the maximum landslide depth. Using such measurements as input data for the ISSM, conservative predictions of slope stability are obtained. The assessment of slope stability involving the ISSM at catchment scale should therefore be considered a regional overview showing potential areas for more detailed investigations. This is particularly important if landslide volumes are of interest, which are generally overestimated by the ISSM when using the maximum regolith depth.

The failure of the 3D models to correctly predict the observed slope failures may be related to the variability of the geotechnical parameters. Sliding surfaces most likely coincide spatially with geotechnically susceptible areas, layers or interfaces, spaced in a more or less irregular way. Even though much effort was put in sampling and testing, it appears hardly feasible to parameterize such patterns of localized patches of low soil strength, increased water input or increased hydraulic conductivity, or the effects of the vegetation (de Lima Neves Seefelder et al. 2016). This means that either even more detailed studies including comprehensive material sampling and testing as well as regolith depth measurements, or appropriate techniques for a stochastic representation of the variability of the key parameters, are necessary for studies of single landslides or slopes.

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