An Improved Singular Value Decomposition Recommender Algorithm Based on User Trust Relationship

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Abstract. Collaborative filtering is one of the most widely used recommender algorithms, whereas it is suffering the issues of data sparsity. Recommender algorithms based on trust perform better in alleviating data sparsity. However, there remain shortages in the process of mining trust relation in specific algorithms, which limit the improvement of prediction accuracy. To address this problem, the paper proposes an improved singular value decomposition algorithm, trying to integrate truster-specific and trustee-specific information and the implicit feedback of each when generating predictions. Experiments on the Epinions dataset show that the proposed algorithm performs better than state-of-the-art recommender algorithms in prediction accuracy.

Introduction

Recommender system has proved to be an effective way to solve the problem of information overload. Specially, collaborative filtering (CF) is a widely used recommendation technology. It generates recommendation for the target user by collecting the preference information of similar users and do not require rich descriptions about users and items. Generally, two types of CF techniques have been investigated: Memory-based and Model-based algorithms. Although CF techniques have been proven effective for recommendations, they still have some limitations on prediction accuracy, including data sparsity and cold-start problems [1].

With the advent of online social network, the data shared among people has provided massive information to describe the real world. Exploiting social networks information in recommender systems has become the new approach of overcoming problems in traditional CF technique [2]. Specially, researches on CF have introduced the trust relationship into recommender systems. The trust relationship is one of the most important types of social information which is based on the idea that people are often influenced by the opinion of the ones they trust in [3]. Incorporating trust into recommender system has proved to be an effective method to improve recommendation performance and to help mitigate the problem of data sparsity and cold-start [4].

However, most of the latest works on trust-based CF algorithms [5] have not taken more detailed trust information, i.e. the implicit influence of trust, into consideration. Consequently, there remains space for the improvement of prediction accuracy.

Aiming at the problems mentioned above, the paper proposes a novel trust-based recommendation model by considering truster-specific and trustee-specific information and the implicit feedback of them when generating predictions. Experimental results on the data set from Epinions.com demonstrate that our approach achieves better accuracy than state-of-the-art CF algorithms.

The rest of this paper is organized as follows: Some related works are discussed in the next section. Then we introduce the improved SVD++ algorithm. Evaluations are discussed in the next section. Finally, we give the conclusion and future work.

Related Work

Basically, two questions needs to be solved when studying trust-based CF algorithm. One is how to obtain trust data and how to evaluate the trust degree. Some researchers estimate the trust relationships between the users from their historical ratings [6,7], which essentially can be regarded as
similarity-based approach [8]. Some other researcher estimate trust from explicit trust statement [5,9,10].

Another question is how to incorporate trust into a specific algorithm. Methods can be classified into two categories. The first category incorporates trust with Memory-based algorithms. Some researchers replace similarity with trust [11]. Guo [12] calculates user similarity based on trust degree and using similarity to generated predictions. Li [6] combines similarity and trust into a unified algorithm using a weighting coefficient. However, simply combination of trust and similarity would not bring significant improvements in prediction accuracy because they have strong correlation. The second category incorporates trust with Memory-based algorithms. Ma [5] proposes the SocialMF matrix factorization algorithm, which involves the influence of trust by incorporating trust into user-specific vector. Yang [13] models truster feature and trustee feature respectively and proposes the TrustMF algorithm. Guo [4] incorporates the explicit and implicit influence of trusted users when generating predictions. However, these works do not mining the influence of trust relationship more deeply, which make it difficult to meet the needs of prediction accuracy in social network recommendation.

The Improved SVD Recommender Algorithm

**Problem Definition.** The paper focuses on the problem of predicting the rating of a user on an unrated item. The input data includes a user-item rating matrix and a user-user trust matrix. Suppose there are m users in the recommender system. That means there exists a trust network with m nodes. Each node represents a user and the directed edges between nodes represent the trust relationship. Let $T = [t_{u,v}]_{m \times m}$ denote the trust network, where each entry $t_{u,v}$ indicates the extent to which user $u$ trusts user $v$.

Definition 1. *Truster-specific feature vector* $t_r^u$, describes the rating feature of user $u$ and how user $u$ trust other users in the system.

Definition 2. *Trustee-specific feature vector* $t_e^v$, describes the rating feature of user $v$ and how user $v$ is trusted by other users in the system.

Hence, the truster feature matrix is represented by $T_r^{d \times m}$, and the trustee feature matrix is represented by $T_e^{d \times m}$. The inner product of a truster-specific vector and trustee-specific vector $t_{r,u}^u \cdot t_{e,v}^v$ can be used to predict the trust relationship between $u$ and $v$. The trust matrix can be recovered by $T = T_r^T T_e$.

**The TSVD++ Model.** In this section, we propose an improved singular value decomposition model TSVD++ based on both truster-specific feature and trustee-specific feature. The TSVD++ model shown as Fig. 1 includes two sub-models: 1) TRSVD++ model that is build based on truster-specific feature; and 2) TESVD++ model that is build based on trustee-specific feature. We perform stochastic gradient descent [14] to learn the parameters in the two sub-models. Then the final parameters are obtained by liner fusion technique.

![TSVD++ model](image)
1) The TRSVD++ Model. A state-of-the-art model known as SVD++ [15] takes user/item biases and the influence of user’s rating behavior. Formally, the user feature is predicted by:

\[ p_u + |I_u| \frac{1}{2} \sum_i x_i. \]  

(1)

Where \( p_u \) represents how user \( u \) rates items, \( |I_u| \) represents the number of items rated by \( u \), \( |I_u| \frac{1}{2} \sum_i x_i \) denotes the implicit feedback of \( u \)’s rating behavior on the rating in the future.

Considering the fact that rating on some items and stating trust in other users are both kinds of opinion given by a user, we can incorporate the implicit feedback of user’s trust behavior on item rating in the same way as SVD++ do, given by [4]:

\[ p_u + |I_u| \frac{1}{2} \sum_i x_i + |T_u| \frac{1}{2} \sum_v y_v. \]  

(2)

where \( p_u \) represents how user \( u \) rates items and how \( u \) trusts other people in the social network, \( |T_u| \) denotes the number of users \( u \) trusted, \( |T_u| \frac{1}{2} \sum_v y_v \) denotes the implicit feedback of \( u \)’s trust behavior on item rating.

For clarity, we rewrite symbol \( p_u \) as \( tr_u \), and \( y_v \) as \( te_v \). Thus, user \( u \)’s rating on item \( j \) is predicted as (3):

\[ \overline{r_{u,j}} = b_u + b_j + \mu + q_y (tr_u + |I_u| \frac{1}{2} \sum_i x_i + |T_u| \frac{1}{2} \sum_v y_v). \]  

(3)

2) The TESVD++ Model. In social network, trust statements on other people reflects part of user’s profile. Actually, the way a user be trusted by other people also reflects part of his profile. Detailedly, we take a simple trust network shown in Fig. 2 as an example. As described in the TRSVD++ model, \( u_1 \) trust \( u_a \) and \( u_b \), then we can draw the conclusion that \( u_a \) and \( u_b \) has the ability to recommender items for \( u_1 \). In fact, consider the user set who trust \( u_a \) and \( u_b \) respectively: \( T_{u_a} = \{ u_1 \} \) and \( T_{u_b} = \{ u_1, u_2, u_3 \} \), suppose \( u_a \), \( u_1 \), and \( u_3 \) has the same credibility, then it can be inferred that \( u_a \) has more ability to recommender items because \( u_b \) is trusted by more people.

![Fig. 2 A simple trust network](image)

Taking the trustee-specific information and the implicit feedback of it into consideration, a novel user feature is predicted by:

\[ te_u + |I_u| \frac{1}{2} \sum_i x_i + |T_{u_b}^*| \frac{1}{2} \sum_v tr_v. \]  

(4)

where \( te_u \) denotes how user \( u \) is trusted by others and how he rates items, \( |I_u| \frac{1}{2} \sum_i x_i \) denotes the implicit feedback of \( u \)’s rating behavior on the rating in the future, \( |T_{u_b}^*| \) denotes the number of users who trust \( u \), \( |T_{u_b}^*| \frac{1}{2} \sum_v tr_v \) denotes the implicit feedback of how \( u \) is trusted by others. The prediction formula is given by:
\[
\overline{r}_{u,j} = b_u + b_j + \mu + q_j^T (p_u + |I_u|) \frac{1}{2} \sum_{a \in I_u} x_a^r + |T_u| \frac{1}{2} \sum_{a \in T_u} x_a^r.
\]  

(5)

3) Description of Algorithm. The steps of TSVD++ algorithm is described below:

Step1: Using the user-user trust matrix \( T \) and the user-item rating matrix \( R \) as the input. Learning the parameters in TRSVD++ model. The objective function is given as (6):

\[
L = \frac{1}{2} \sum_{u \in U} (\overline{r}_{u,j} - r_{u,j})^2 + \frac{\lambda}{2} \sum_{u \in U} \sum_{a \in I_u} (\overline{\overline{r}_{u,j}} - \overline{r}_{u,j})^2 + \frac{\lambda}{2} \sum_{j \in J} (\overline{b_j^t} + \overline{b_j^r}) + \sum_{u \in U} \| \overline{t_u} \|_F^2 + \sum_{v \in V} \| \overline{t_v} \|_F^2 + \sum_{q \in Q} \| \overline{q} \|_F^2 + \sum_{x \in X} \| X \|_F^2 + \frac{\lambda}{2} \sum_{u \in U} \| \overline{t_u} \|_F^2.
\]  

(6)

where \( \overline{t_{u,j}} = t_{u,j}^T \overline{t_u} \), \( \lambda \) and \( \lambda_e \) are regularization parameters to avoid over-fitting. Stochastic gradient descent is applied to learn parameters \( b_u, b_j, q_j, x_i, t_{u,r} \) and \( t_{e,v} \).

Step2: Using the user-user trust matrix \( T \) and the user-item rating matrix \( R \) as the input. Learning the parameters in TESVD++ model in the same way as in Step1. The objective function is given as (7):

\[
L = \frac{1}{2} \sum_{u \in U} (\overline{r}_{u,j} - r_{u,j})^2 + \frac{\lambda}{2} \sum_{u \in U} \sum_{a \in I_u} (\overline{\overline{r}_{u,j}} - \overline{r}_{u,j})^2 + \frac{\lambda}{2} \sum_{j \in J} (\overline{b_j^t} + \overline{b_j^r}) + \sum_{u \in U} \| t_{u,j} \|_F^2 + \sum_{v \in V} \| t_{v,j} \|_F^2 + \sum_{q \in Q} \| q_j \|_F^2 + \sum_{x \in X} \| x_i \|_F^2 + \frac{\lambda}{2} \sum_{u \in U} \| \overline{t_u} \|_F^2.
\]  

(7)

where \( t_{u,j} = t_{u,j}^t \overline{t_u} \), and the parameters are \( b_u, b_j, q_j, x_i, t_{u,r} \) and \( t_{e,v} \).

Step3: Liner fusion of the parameters learned from TRSVD++ and TESVD++.

\[
b_u^* = \frac{b_u + b_u'}{2}.
\]  

(8)

\[
b_j^* = \frac{b_j + b_j'}{2}.
\]  

(9)

\[
p_u^* = \frac{t_{u,r} + t_{e,v}}{2}.
\]  

(10)

\[
q_j^* = \frac{q_j + q_j'}{2}.
\]  

(11)

\[
x_i^* = \frac{x_i + x_i'}{2}.
\]  

(12)

Finally, the rating formula of TSVD++ algorithm is given as (13):

\[
\overline{r}_{u,j} = b_u^* + b_j^* + \mu + q_j^T (p_u + |I_u|) \frac{1}{2} \sum_{a \in I_u} x_a^r + |T_u| \frac{1}{2} \sum_{a \in T_u} x_a^r.
\]  

(13)

Experiments and Results

Dataset. We use the dataset from Epinions.com [16] in the experiments. The data set contains 40163 users and 139738 items. The number of ratings is 664824. The number of trustees and trustees are 33960 and 49288, and the number of trust relationship is 487183. The ratings range from 1 to 5. The trust statements are binary, including trust (1) and distrust (-1).

Evaluation Metrics. We use Mean Absolute Error (MAE) and root mean square error (RMSE) to evaluate the performance of different recommendation algorithms. In general, lower MAE and RMSE mean better predictive accuracy.

\[
MAE = \frac{1}{|S_{test}|} \sum_{(u,j) \in S_{test}} | \overline{r}_{u,j} - r_{u,j} |.
\]  

(14)

\[
RMSE = \sqrt{\frac{1}{|S_{test}|} \sum_{(u,j) \in S_{test}} (\overline{r}_{u,j} - r_{u,j})^2}.
\]  

(15)

Where \( S_{test} \) is the testing set and \( |S_{test}| \) is the number of user-item pairs.

Comparison Methods. To evaluate the performance of TSVD++ method, 3 categories of comparison CF methods are selected:

Memory-based baselines: UserMean and ItemMean, mean rating of users and items respectively.

Model-based CF: SVD++ [15], PMF [17].

Trust-based CF: TrustSVD [4], SocialMF [5], TrustMF [13].
The optimal experimental settings for comparison methods are suggested by previous work, as shown in Table 1.

| Methods    | Optical Parameters |
|------------|--------------------|
| PMF        | λ=λ, =0.001        |
| SVD++      | λ=0.35             |
| SocialMF   | λ = 0.001, λ = 1   |
| TrustMF    | λ = 0.001, λ = 1   |
| TrustSVD   | λ = 0.9, λ = 0.5   |

In the evaluations, 5-folder crossing validation is used. In each time, we select 80% of data as training set and the rest of 20% for test. The results are the arithmetical average of the 5 tests.

**Validation on Prediction Accuracy.** In the experiments, we set the number of latent features d=5 and d=10 [4, 10, 13], learning rate=0.001 [4]. To prevent infinite iteration, we set the experimental maximum number of iterations to be 100. The optimal parameter settings for TSVD++ are λ = 0.08, λ = 0.6.

The experimental results are shown in Table 2. TrustSVD performs the best for all comparison method. These results are consistent with Guo’s conclusion [4]. On the contrary, our approach TSVD++ outperforms the comparison methods. Specifically, 1.10% improvements in MAE when d=5, and 0.82% when d=10. 1.01% improvements in RMSE when d=5, and 0.69% when d=10. Some explanations can be made: In the comparison methods, the baseline and model based algorithms do not make use of the trust information. SocialMF exploits the explicit trust statements but fails to consider the implicit feedback of them. TrustMF incorporates both truster-specific and trustee-specific information but without their implicit feedback. TrustSVD exploits truster-specific information and their implicit feedback but fails to consider trustee-specific feature. However, our approach integrates truster-specific and trustee-specific information and the implicit feedback of each when generating predictions. In a word, our approach takes advantage of the mentioned comparison methods, and performs better in predictive accuracy.

| Metrics | UserMean | ItemMean | PMF | SVD++ | SocialMF | TrustMF | TrustSVD | TSVD++ | Improvement |
|---------|----------|----------|-----|-------|----------|---------|----------|--------|-------------|
| d=5     | 0.936    | 0.933    | 0.986 | 0.824 | 0.832    | 0.823   | 0.810    | 0.802  | 1.10%       |
| d=10    | 0.936    | 0.933    | 1.035 | 0.824 | 0.833    | 0.826   | 0.811    | 0.803  | 1.01%       |

**Conclusion and Future Work**

This paper proposed an improved SVD-based recommendation algorithm TSVD++ that incorporates truster-specific and trustee-specific information and the implicit feedback of them in the process of rating prediction. The experimental results in real world dataset prove that TSVD++ outperforms conventional CF methods in predictive accuracy. In the future, we plan to improve the model by adapting the weighted regularization technique. In the meantime, we will also look into better method in parameter fusion to reduce the complexity of the algorithm.

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