Diffraction-free optical beam propagation with near-zero phase variation in extremely anisotropic metamaterials

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Abstract

Extremely anisotropic metal-dielectric multilayer metamaterials are designed to have the effective permittivity tensor of a transverse component (parallel to the interfaces of the multilayer) with zero real part and a longitudinal component (normal to the interfaces of the multilayer) with ultra-large imaginary part at the same wavelength, including the optical nonlocality analysis based on the transfer-matrix method. The diffraction-free deep-subwavelength optical beam propagation with near-zero phase variation in the designed multilayer stack due to the near-flat iso-frequency contour is demonstrated and analyzed, including the effects of the multilayer period and the material loss.

Keywords: multilayer metamaterials, extreme anisotropy, diffraction-free near-zero phase variation propagation, optical nonlocality

1. Introduction

Light beam propagating beyond diffraction limit with deep-subwavelength confinement and near-zero phase variation is highly desirable in many optical integration applications. In order to realize such intriguing optical beam propagation phenomena, optical materials are required to possess an extremely anisotropic effective refractive index tensor with an ultra-high component perpendicular to the propagation direction to support the light beam of large wave vector and an ultra-low component in the propagation direction to reduce the phase variation of the light beam simultaneously. Optical metamaterials with artificial subwavelength meta-atoms and tunable effective permittivity and effective permeability have been designed to exhibit ultra-high effective refractive index so as to achieve large wave vectors [1, 2], as well as to have zero effective refractive index for obtaining the optical beam propagation with zero phase variation [3, 4]. Among all these designs, the metal-dielectric multilayer metamaterials are of great interest in demonstrating many exciting applications such as negative refraction [5], epsilon-near-zero (ENZ) materials [6–9], and epsilon-near-pole (ENP) materials [10]. Particularly, possessing an indefinite permittivity tensor, the multilayer metamaterials are of unique applications in sub-wavelength imaging [11, 12], enhanced photonic density of states [13], broadband light absorbers [14–16], ultra-high refractive indices for subwavelength optical waveguides [17], indefinite cavities [18, 19], broadband spontaneous emission engineering [20–22], super-Plank thermal emission [23–25], ultra-large-wavevector plasmon polaritons [26–28], and other exceptional properties [29–31].

In our previous work [32], the extremely loss-anisotropic metal-dielectric multilayer metamaterials are designed in order to realize the diffraction-free optical beam propagation mainly based on the effective medium theory (EMT) and the operation wavelength is adjusted from the dispersion relation of the multilayer stack. However, the effective permittivity tensor including the optical nonlocality is not well considered in the analysis. Therefore, in the present work, a new kind of metal-dielectric multilayer
metamaterials are designed to have the extremely anisotropic effective permittivity tensor for the demonstration of both the diffraction-free optical beam propagation and the near-zero phase variation along the propagation direction, based on a theoretical analysis of the effective permittivity tensor including the optical nonlocality. The designed multimaterial metamaterials will have the effective permittivity tensor with a near-zero transverse component parallel to the multilayer and an ultra-large longitudinal component in the imaginary part normal to the multilayer at the same wavelength, which represents the ENZ–ENP wavelength. The near-zero transverse component of the effective permittivity tensor leads to the near-zero phase variation during the propagation of the electromagnetic wave. On the other hand, the longitudinal component with an ultra-large imaginary part of the effective permittivity tensor will reduce the diffraction of the electromagnetic wave [33, 34]. The filling ratio of metal in the metal-dielectric multilayer stack with respect to the ENZ–ENP wavelength is fully analyzed according to the transfer-matrix method including the optical nonlocality, while the performance of the deep-subwavelength optical beam propagation with near-zero phase variation is also explored with respect to the variation of the material loss. In the following sections, the diffraction-free optical beam propagation with near-zero phase variation is discussed in theoretical analysis based on EMT and optical nonlocality, together with numerical simulation in section 2, followed by the conclusion in section 3.

2. Theory and discussion

2.1. EMT and optical nonlocality

Illustrated in figure 1(a), the metal-dielectric multilayer stack is composite of alternating layers of silver (Ag) and titanium pentoxide (Ti3O5), with the thickness $a_m$ and $a_d$, respectively. The permittivity of Ag follows the Drude model

$$\varepsilon_m = \varepsilon_\infty - \frac{\omega_p^2}{(\omega^2 + i\omega\gamma)}$$

with the permittivity constant $\varepsilon_\infty = 5.7$, the plasma frequency $\omega_p = 1.37 \times 10^{16}$ rad s$^{-1}$, and the damping factor $\gamma = \Delta \cdot (8.5 \times 10^{13})$ rad s$^{-1}$. According to the previous experimental demonstration [35], the material loss of Ag can be reduced by the annealing process so that the damping factor $\gamma$ is decreased. Here the damping factor $\Delta$ is included in order to tune the material loss of Ag and is set to be $\Delta = 0.1$ in the following analysis. The permittivity of Ti3O5 is $\varepsilon_d = 5.83$. When the thickness of each layer is sufficiently small, i.e., $|ka| \ll 1$, where $k$ is the wave vector in the layer and $a$ is the thickness of the layer [36], the multilayer stack can be regarded as a homogeneous anisotropic effective medium with a permittivity tensor based on the EMT

$$\varepsilon_{xy}^{EMT} = \varepsilon_m \varepsilon_m + \frac{f_d}{f_d} \varepsilon_d,$$

$$\varepsilon_z^{EMT} = \left(\frac{f_m}{\varepsilon_m} + \frac{f_d}{\varepsilon_d}\right)^{-1},$$

which is related to the filling ratio of Ag and Ti3O5, $f_m = a_m/(a_m + a_d)$ and $f_d = a_d/(a_m + a_d)$. According to equation (1), it is interesting that if the real part of the permittivity of Ag is greater than that of the imaginary part, i.e., $\text{Re}(\varepsilon_m) > \text{Im}(\varepsilon_m)$, the EMT-based ENZ wavelength (where $\text{Re}(\varepsilon_{xy}^{EMT}) = 0$) and the EMT-base ENP wavelength (where the maximum of $\text{Im}(\varepsilon_{xy}^{EMT})$ is obtained) can be approximately associated with the EMT-based filling ratio of Ag as $f_m^{EMT} \approx \varepsilon_d/(\varepsilon_d - \varepsilon_m)$ and $f_d^{EMT} \approx -\text{Re}(\varepsilon_m)/(\varepsilon_d - \text{Re}(\varepsilon_m))$, respectively. Therefore, the EMT-based ENZ–ENP wavelength is related to the approximate condition of $\varepsilon_d = -\text{Re}(\varepsilon_m)$, which implies that once the EMT-based ENZ wavelength overlaps with the EMT-based ENP wavelength, the EMT-based filling ratio of Ag should be $f_m^{EMT} \approx 1/2$. Further algebraic calculation indicates that the accuracy result of the EMT-based filling ratio of Ag is $f_m^{EMT} = 0.500$, with respect to the permittivity of Ag in terms of Drude model and the permittivity of Ti3O5. Correspondingly, the EMT-based effective permittivity tensor reads $\varepsilon_{xy}^{EMT} = 0.000 + 0.012i$ and $\varepsilon_z^{EMT} = 7.238 + 2798.497i$, presenting an extremely anisotropic permittivity property of the multilayer stack. Regarding a TM-polarized light with non-vanishing $E_x, H_y$, and $E_z$ field components propagating along the $z$-direction in the $x$-$z$ plane, the iso-frequency contour (IFC) of the multilayer stack reads

$$k_z^2/\varepsilon_z^{EMT} + k_x^2/\varepsilon_{xy}^{EMT} = k_0^2,$$

while considering the extremely anisotropic permittivity property, i.e., $|\varepsilon_{xy}^{EMT}| \gg 1 \gg |\varepsilon_z^{EMT}| \approx 0$ at the EMT-based ENZ–ENP wavelength, the IFC equation in equation (2) can be approximately written as

$$k_z/k_0 = \sqrt{\varepsilon_{xy}^{EMT}} \left(1 - (k_z/k_0)^2/\varepsilon_z^{EMT}\right)^{1/2} \approx \sqrt{\varepsilon_{xy}^{EMT}} - \sqrt{\varepsilon_{xy}^{EMT}} \left(k_z/k_0\right)^2/\left(2\varepsilon_z^{EMT}\right).$$

Therefore, as shown in figure 1(b), according to equation (3), the IFC of the multilayer stack at the EMT-based ENZ–ENP wavelength forms flat lines of the value $k_z/k_0 \approx (\varepsilon_{xy}^{EMT})^{1/2}$ with respect to a wide $k_z/k_0$ wave vector range, which leads to a diffraction-free optical beam propagation in the multilayer stack since all spatial components propagate with the same phase velocity along the $z$-direction. Furthermore, due to the fact that $\text{Re}(\varepsilon_{xy}^{EMT}) = 0$ and $\varepsilon_{xy}^{EMT} \ll 1$, the phase variation of the diffraction-free optical beam propagation in the multilayer stack is close to zero.

However, previous studies show that the metal-dielectric multilayer stack possesses strong optical nonlocality [36–39], leading to the effective permittivity tensor not only related to the frequency but also to the wave vector, especially when the frequency approaches to the ENZ position of the structure. Such optical nonlocality can be analyzed via the transfer-matrix method, in which the multilayer stack is considered as a one-dimensional photonic crystal with the dispersion
relation to the TM-polarized light as
\[
\begin{align*}
\cos(k_z(m + a)) &= \cos(k_m a)(k_m) + k_d d_k \\
&= -\left(\epsilon_m k_d / \epsilon_d k_m + \epsilon_k m k_m / \epsilon_k d d_k / 2 \right) \\
&\times \sin(k_m a) \sin(k_d a),
\end{align*}
\]

with the wave vector \( k_z = \sqrt{\epsilon_k k_0^2 - k_i^2} \) for \( i = m, d \). Accordingly, the effective permittivity component in \( x \)- and \( y \)-direction including the optical nonlocality reads
\[
\epsilon_{xy}^{\text{nonloc}} = \arccos\left[\frac{\sin(\sqrt{k_m k_0 a_m}) + \cos(\sqrt{k_d k_0 a_d})}{(k_m^2 (a_m + a_d)^2 - k_i^2)}\right].
\]

On the other hand, the nonlocal effective permittivity component in the \( z \)-direction can be analytically obtained according to the effective permittivity definition \( \epsilon_{z}^{\text{nonloc}} = \langle D_z \rangle / \langle E_z \rangle \) based on the transfer-matrix method. Due to the optical nonlocality, the nonlocal ENZ wavelength and the nonlocal ENP wavelength for the multilayer stack will be different from the EMT-based ENZ–ENP wavelength. Therefore, modification on the multilayer geometry is necessary for a certain period of \( a_m + a_d = 20 \) nm. Compared with the EMT results, the nonlocal results clearly indicate the shift of the ENZ–ENP wavelength from the EMT calculated position of \( \lambda_{\text{EMT}} = 466.896 \) nm to the new position of \( \lambda_{\text{nonloc}} = 468.424 \) nm, while the nonlocal effective permittivity components are \( \epsilon_{xy}^{\text{nonloc}} = 0.000 + 0.012i \) and \( \epsilon_{z}^{\text{nonloc}} = 7.214 + 2800.879i \). Furthermore, the filling ratio of Ag related to the optical nonlocality (nonlocal filling ratio for short) also slightly changes to \( f_m^{\text{nonloc}} = 0.51 \), with respect to the period of the multilayer stack. In more detail, figures 2(a) and (b) individually display the variations of the filling ratio of Ag and the ENZ–ENP wavelength with respect to different periods of the multilayer stack caused by the optical nonlocality. For comparison, the EMT results are also plotted. It is clear that as the multilayer stack period gets larger, the nonlocal filling ratio of Ag increases and the nonlocal ENZ–ENP wavelength also shifts to a longer wavelength.

**2.2. Diffraction-free and near-zero phase variation propagation**

Based on the finite element method, the diffraction-free optical beam propagation with near-zero phase variation is demonstrated according to the numerical simulation in terms of two anti-phase TM-polarized Gaussian beams that are excited via the stimulating port boundary condition with an initial electric field distribution following the Gaussian
distribution function as \( \exp\left(-\left(x + c_0\right)^2/w_0^2\right) \), where \( c_0 \) determines the beam centre and \( w_0 \) determines the waist size. Otherwise, the scattering boundary condition is applied to prevent the unwanted scattering from other boundaries of the simulation region. The simulation results are presented as the amplitude of the electric field, normalized by the maximum value. Figure 3 shows the calculated optical beam propagation of the Gaussian beams with ultra-narrow beam waists of \( w_0 = 25 \) nm in the homogeneous anisotropic effective medium at the EMT-based ENZ–ENP wavelength of \( \lambda_{cEMT} = 466.896 \) nm. Besides, figure 4 shows the optical beam propagation results calculated in the 20 nm period multilayer stack at the nonlocal ENZ–ENP wavelength \( \lambda_{cnonloc} = 468.424 \) nm. As shown in figures 3(a) and 4(a), it is...
clear that the deep-subwavelength Gaussian beams can propagate over a long distance (\(>2\Delta_{\text{nonloc}}\)) without any wave front distortion. At the same time, near-zero phase variation is also obtained along the propagation direction. The centre-to-centre distance of 120 nm for the two deep-subwavelength Gaussian beams remains well-defined as the beams propagating across the multilayer stack from the bottom to the top. It is noted that the confinement and propagation of the deep-subwavelength Gaussian beam inside the multilayer stack is entirely due to the unique extremely anisotropic permittivity property, and the optical beam path is well determined by the beam launching position, which is distinguished from the situation in a subwavelength optical waveguide [17], where the optical mode is confined by the waveguide boundary. Besides the straight optical beam propagation, the flow of light can be flexibly modeled through controlling the local geometry of the multilayer stack. For instance, the beam path can be manipulated by gradually varying the direction of multilayers, since the direction of the optical beam propagation is always vertical to the multilayer interface. The designed geometries for achieving 90° and 180° bending of deep-subwavelength Gaussian beams and the simulation results are shown in figures 3(b) and (c) and 4(b) and (c), for the effective medium and the multilayer stack, respectively. It is noted that for the effective medium the anisotropic effective permittivity tensor is transformed according to the geometric relation between the global xyz-coordinates and the local uwv-coordinates based on the transformation optics as

\[
\epsilon_{\text{eff}}(x, z) = \begin{pmatrix} 
\epsilon_u \cos^2 \theta + \epsilon_w \sin^2 \theta & (\epsilon_u - \epsilon_w) \sin \theta \cos \theta \\
(\epsilon_u - \epsilon_w) \sin \theta \cos \theta & \epsilon_u \sin^2 \theta + \epsilon_w \cos^2 \theta 
\end{pmatrix}. 
\tag{6}
\]

The results indicate that the flow of light can indeed be manipulated while maintaining the diffraction-free propagation with near-zero phase variation. For comparison, figure 4(d) presents the optical beam propagation at the wavelength of \(\lambda = 464\) nm, which is off the nonlocal ENZ–ENP wavelength of the 20 nm period multilayer stack, while the corresponding nonlocal effective permittivity components read

\[
\epsilon_{\text{xy}}^\text{nonloc} \bigg|_{\lambda=464\text{ nm}} = 0.121 + 0.012i \\
\epsilon_{\text{zz}}^\text{nonloc} \bigg|_{\lambda=464\text{ nm}} = -336.266 + 42.895i.
\]

It is clear that by overlapping the ENZ wavelength and the ENP wavelength, the multilayer stack with such an extremely anisotropic effective permittivity tensor supports diffraction-free propagation with near-zero phase variation. Also, it implies that the diffraction-free propagation supported by the anisotropic effective permittivity tensor is not extremely sensitive to the value of wavelength, but for the near-zero phase variation, the ENZ wavelength must be satisfied.

In the previous analysis, the damping factor ratio of Ag is set as \(\Delta = 0.1\) in order to maintain a small material loss to extend the propagation distance of the Gaussian beams. In fact, the variation of the damping factor in the Drude model will affect the optical beam propagation loss and the phase variation. Figure 5(a) represents the variation of the propagation length and the effective refractive index along the propagation direction with respect to different damping factor ratios of Ag. The effective refractive index is defined based on the nonlocal effective permittivity component as

\[
\Delta R_{\text{eff}} \bigg|_{\lambda=464\text{ nm}} = \frac{\epsilon_{\text{xy}}}{\epsilon_{\text{zz}}} \bigg|_{\Delta=0.1, 0.5, 1.0}
\]

The real part of the effective refractive index \(\Re(n_{\text{eff}})\) is proportional to the phase variation of the propagating beam, while the imaginary part \(\Im(n_{\text{eff}})\) is inversely proportional to the propagation length of the beam as \(\lambda/(4\pi \Im(n_{\text{eff}}))\), where \(\lambda\) is the wavelength of the beam in free space. It is clear that as the damping factor ratio of Ag gets larger, the real part of the effective refractive index increases, leading to an obvious beam phase variation along the propagation direction. On the other hand, the propagation length also decreases as the material loss gets higher. Figures 5(b)–(d) show the propagation of the two anti-phase Gaussian beams in the 20 nm period multilayer stack with different damping factor ratio of \(\Delta = 0.1, 0.5, 1.0\) at the nonlocal-based ENZ–ENP wavelengths.

Finally, it is worth mentioning that according to the previous experimental work of optical hyperlens [11], our
above theoretical analysis of extremely anisotropic metamaterials can be realized in experiments. The ultra-narrow Gaussian beams can be achieved by inscribing nanometer scale slots or holes into a thin chrome layer coated on the top of the sample surface, while the impedance matching substrate can be applied at the bottom of the multilayer stack in order to reduce the reflection caused by the mismatched impedance.

3. Conclusions

To conclude, extremely anisotropic metal-dielectric multilayer metamaterials with identical ENZ wavelength and ENP wavelength have been designed based on the transfer-matrix method including the optical nonlocality. Such metamaterial possesses a near-flat IFC with wave vector values close to zero over a broad wave vector range. This unique property is utilized to obtain the diffraction-free deep-subwavelength optical beam propagation with near-zero phase variation, and it is demonstrated that the optical beam propagation can be manipulated flexibly by tuning the direction of the multilayer stack. The influences of multilayer period and material loss on the optical beam propagation are also studied. The current study is of great potentials in many applications such as optical imaging, optical integration, and on-chip optical communication.

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References

[1] Shin J, Shen J T and Fan S 2009 Three-dimensional metamaterials with an ultrahigh effective refractive index over a broad bandwidth Phys. Rev. Lett. 102 093903
[2] Choi M, Lee S H, Kim Y, Kang S B, Shin J, Kwak M H, Kang K Y, Lee Y H, Park N and Min B 2011 A terahertz metamaterial with unusually high refractive index Nature 470 369–73
[3] Huang X, Lai Y, Hang Z H, Zheng H and Chan C T 2011 Dirac cones induced by accidental degeneracy in photonic crystals and zero-refractive-index materials Nat. Mater. 10 582–6
[4] Vesseur E J R, Coenen T, Caglayan H, Engheta N and Polman A 2013 Experimental verification of n = 0 structures for visible light Phys. Rev. Lett. 110 013902
[5] Valentine J, Zhang S, Zentgraf T, Ulin-Avila E, Genov D A, Bartal G and Zangh X 2008 Three-dimensional optical metamaterial with a negative refractive index Nature 455 376–9
[6] Maas R, Parsons J, Engheta N and Polman A 2013 Experimental realization of an epsilon-near-zero metamaterial at visible wavelengths Nat. Photonics 7 907–12
[7] Gao J, Sun L, Deng H, Mathai C J, Gangopadhyay S and Yang X 2013 Experimental realization of epsilon-near-zero metamaterial slabs with metal-dielectric multilayers Appl. Phys. Lett. 103 051111
[8] Sun L, Gao J and Yang X 2013 Giant optical nonlocality near the Dirac point in metal-dielectric multilayer metamaterials Opt. Express 21 21542–55
[9] Sun L, Cheng F, Mathai C J, Gangopadhyay S, Gao J and Yang X 2014 Experimental characterization of optical nonlocality in metal-dielectric multilayer metamaterials Opt. Express 22 22974–80
[10] Molesky S, Dewalt C J and Jacob Z 2013 High efficient epsilon-near-zero and epsilon-near-pole metamaterial emitters for thermophotovoltaics Opt. Express 21 96–110
[11] Liu Z, Lee H, Xiong Y, Sun C and Zhang X 2007 Far-field optical hyperlens magnifying sub-diffraction-limited objects Science 315 1666
[12] Zhang X and Liu Z 2008 Superlenses to overcome the diffraction limit Nat. Mater. 7 435–41
[13] Krishnamoorthy H N S, Jacob Z, Narimanov E, Kretzschmar I and Menon V M 2012 Topological transitions in metamaterials Science 336 205–9
[14] Cui Y, Fung K H, Xu J, Ma H, Jin Y, He S and Fang N X 2012 Ultrabroadband light absorption by a sawtooth anisotropic metamaterial slab Nano Lett. 12 1443–7
[15] Guclu C, Campione S and Capolino F 2012 Hyperbolic metamaterial as a super absorber for scattered fields generated at its surface Phys. Rev. B 86 205130
[16] Narimanov E E, Li H, Barnakov Yu A, Tumkur T U and Noginov M A 2013 Reduced reflection from roughened hyperbolic metamaterial Opt. Express 21 14956–61
[17] He Y, He S, Gao J and Yang X 2012 Nanoscale metamaterial optical waveguides with ultrahigh refractive indices J. Opt. Soc. Am. B 29 2559–66
[18] Yao J, Yang X, Yin X, Bartal G and Zhang X 2011 Three-dimensional nanometer-scale optical cavities of indefinite medium Proc. Natl Acad. Sci. USA 108 11327–31
[19] Yang X, Yao J, Rho J, Yin X and Zhang X 2012 Experimental realization of three-dimensional indefinite cavities at the nanoscale with anomalous scaling laws Nat. Photonics 6 450–4
[20] Noginov M A, Li H, Barnakov Yu A, Dryden D, Nataraj G, Zhu G, Bonner C E, Mayy M, Jacob Z and Narimanov E E 2010 Controlling spontaneous emission with metamaterials Opt. Lett. 35 1863–5
[21] Kidwai O, Zhukovsky S V and Sipe J E 2011 Dipole radiation near hyperbolic metamaterials: applicability of effective-medium approximation Opt. Lett. 36 2530–2
[22] Jacob Z, Smolyaninov I I and Narimanov E E 2012 Broadband Purcell effect: radiative decay engineering with metamaterials Appl. Phys. Lett. 100 181105
[23] Biels S-A, Tschikin M and Ben-Abdallah P 2012 Hyperbolic metamaterials as an analog of a blackbody in the near field Phys. Rev. Lett. 109 104301
[24] Guo Y, Cortes C L, Molesky S and Jacob Z 2012 Broadband super-Planckian thermal emission from hyperbolic metamaterials Appl. Phys. Lett. 101 131106
[25] Guo Y and Jacob Z 2013 Thermal hyperbolic metamaterials Opt. Express 21 15014–9
[26] Othman M A K, Guclu C and Capolino F 2013 Graphene/dielectric composite metamaterials: evolution from elliptic to hyperbolic wavevector dispersion and the transverse epsilon-near-zero condition J. Nanophotonics 7 073089
[27] Zhukovsky S V, Kidwai O and Sipe J E 2013 Physical nature of volume plasmon polaritons in hyperbolic metamaterials Opt. Express 21 14982–7

[28] Zhukovsky S V, Andryieuski A, Sipe J E and Lavrinenko A V 2014 From surface to volume plasmons in hyperbolic metamaterials: general existence conditions for bulk high-k waves in metal-dielectric and graphene-dielectric multilayers Phys. Rev. B 90 155429

[29] Cortes C L, Newman W, Molesky S and Jacob Z 2012 Quantum nanophotonics using hyperbolic metamaterials J. Opt. 14 063001

[30] Poddubny A, Iorsh I, Belov P and Kivshar Y 2013 Hyperbolic metamaterials Nat. Photonics 7 948–57

[31] Orlov A A, Zhukovsky S V, Iorsh I V and Belov P A 2014 Controlling light with plasmonic multilayers Photonics Nanostruct. 12 213–30

[32] He Y, Sun L, He S and Yang X 2013 Deep subwavelength beam propagation in extremely loss-anisotropic metamaterials J. Opt. 15 055105

[33] Feng S 2012 Loss-induced omnidirectional bending to the normal in $\epsilon$-near-zero metamaterials Phys. Rev. Lett. 108 193904

[34] Sun L, Feng S and Yang X 2012 Loss enhanced transmission and collimation in anisotropic epsilon-near-zero metamaterials Appl. Phys. Lett. 101 241101

[35] Chen W, Thoreson M D, Ishii S, Kildishev A V and Shalaev V M 2010 Ultra-thin ultra-smooth and low-loss silver films on a germanium wetting layer Opt. Express 18 5124–34

[36] Elser J, Podolskiy V A, Salakhutdinov I and Avrutsky I 2007 Nonlocal effects in effective-medium response of nanolayered metamaterials Appl. Phys. Lett. 90 191109

[37] Orlov A A, Voroshilov P M, Belov P A and Kivshar Y S 2011 Engineered optical nonlocality in nanostructured metamaterials Phys. Rev. B 84 045424

[38] Chebykin A V, Orlov A A, Vozianova A V, Maslovski S I, Kivshar Yu S and Belov P A 2011 Nonlocal effective medium model for multilayered metal-dielectric metamaterials Phys. Rev. B 84 115438

[39] Chebykin A V, Orlov A A, Simovski C R, Kivshar Yu S and Belov P A 2012 Nonlocal effective parameters of multilayered metal-dielectric metamaterials Phys. Rev. B 86 115420