A diagrammatic analysis of two-body charmed baryon decays with flavor symmetry

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ABSTRACT: We study the two-body anti-triplet charmed baryon decays based on the diagrammatic approach with SU(3) flavor symmetry. We extract the two $W$-exchange effects as $E_B$ and $E'$ that contribute to the $\Lambda_c^+ \to \Xi^0 K^+$ decay, together with the relative phases, where $E_B$ gives the main contribution. Besides, we find that $\mathcal{B}(\Lambda_c^+ \to p\pi^0) = (0.8^{+0.9}_{-0.8}) \times 10^{-4}$, which is within the experimental upper bound. Particularly, we obtain $\mathcal{B}(\Xi_c^+ \to \Xi^0 \pi^+) = (9.3 \pm 3.6) \times 10^{-3}$, $\mathcal{B}(\Xi_c^0 \to \Xi^- \pi^+, \Lambda^0 K^0) = (19.3 \pm 2.8, 8.3 \pm 5.0) \times 10^{-2}$ and $\mathcal{B}(\Xi_c^0 \to \Xi^- K^+) = (5.6 \pm 0.8) \times 10^{-4}$, which all agree with the data. For the singly Cabibbo suppressed $\Lambda_c^+$ decays, we predict that $\mathcal{B}(\Lambda_c^+ \to n\pi^+, p\eta', \Sigma^+ K^0) = (7.7 \pm 2.0, 7.1\pm1.4, 19.1\pm4.8) \times 10^{-4}$, which are accessible to the experiments at BESIII, BELLEII and LHCb.

KEYWORDS: Branching fraction, Charm physics, Flavor physics, Rare decay, \textit{e+e- Experiments}

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1 Introduction

The experimental studies of two-body $B_c \rightarrow BM$ decays have provided important information for the theoretical understanding of the hadronization in the weak interaction, where $B_c = (\Sigma_c^0, \Xi_c^+, \Lambda_c^+)$ are the lowest-lying anti-triplet charmed baryon states, and $B(M)$ the baryon (meson) state. For example, the BESIII collaboration has recently measured the purely non-factorizable decays, of which the branching fractions are given by

$$B(\Sigma^+_c \rightarrow \Xi^0 K^+) = (5.90 \pm 0.86 \pm 0.39) \times 10^{-3},$$
$$B(\Lambda^+_c \rightarrow \Xi^{*0} K^+) = (5.02 \pm 0.99 \pm 0.31) \times 10^{-3},$$

with $\Xi^{*0} \equiv \Xi(1530)^0$. This implies that the non-factorizable effects can be as significant as the factorizable ones in $B_c \rightarrow BM$ [2, 3], although being often neglected in the b-hadron decays [4–7].

Some theoretical approaches have tried to deal with the non-factorizable effects [8–12]. Nonetheless, $B(\Lambda^+_c \rightarrow \Xi^0 K^+)$ is calculated to be 2–6 times smaller than the observation. Without involving the detailed dynamics, the approach based on the SU(3) flavor (SU(3)$_f$) symmetry is able to receive all contributions [13–31], such that $B(B_c \rightarrow BM)$ can be explained [22–25]: particularly, $B(\Lambda^+_c \rightarrow \Xi^0 K^+)$. However, the SU(3)$_f$ symmetry mixes the factorizable and non-factorizable effects, instead of quantifying their individual contributions.

As depicted in figure 1, one can identify the (non-)factorizable effects by the topological diagrams, and parameterize them as the topological amplitudes [32–34]. Accordingly, $\Lambda^+_c \rightarrow \Xi^{*0} K^+$ is seen to decay through the two $W$-exchange ones in figures 1(d,e). Since the topological diagrams have been commonly used in the calculations and measurements [1, 8–12, 32, 35, 36], their information can be important. Therefore, we propose to perform the numerical analysis with the topological amplitudes, such that we can determine the sizes and relative phases for the different effects. Note that the same numerical analysis known as the diagrammatic approach has been well performed to extract the topological amplitudes in the $D$ decays [37–42]. In this paper, we will demonstrate that
Figure 1. Topological diagrams for the $B_c \rightarrow BM$ decays.

the topological amplitudes can explain the data. Particularly, in our fit we will be able to accommodate the experimental measurements of $\mathcal{B}(\Lambda_c^+ \rightarrow p \pi^0) < 2.7 \times 10^{-4}$ [3] and $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- K^+)/\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+) = (0.56 \pm 0.12)s_c^2$ [43], where $s_c = V_{us}$. We will also predict the branching fractions for the $B_c \rightarrow BM$ decays that have not been observed yet.

2 Diagrammatic approach

For the two-body charmed baryon decays, the relevant effective Hamiltonian is given by [44]

$$\mathcal{H}_{\text{eff}} = \sum_{i=1,2} \frac{G_F}{\sqrt{2}} c_i (V_{cs}V_{ud}O_{1i} + V_{cq}V_{uq}O_{2i} + V_{cd}V_{us}O_{3i}),$$

(2.1)

with $q = (d,s)$, where $G_F$ is the Fermi constant, $c_{1,2}$ are the Wilson coefficients, and $V_{ij}$ the CKM matrix elements. The four-quark operators $O_{1,2}^{(q)}$ and $O_{1,2}'$ are written as

$$O_1 = (\bar{u}d)(\bar{s}c), \quad O_2 = (\bar{s}d)(\bar{u}c),$$

$$O_1' = (\bar{u}q)(\bar{q}c), \quad O_2' = (\bar{q}q)(\bar{u}c),$$

(2.2)

with $q = (d,s)$ and $(\bar{q}_1 q_2) = \bar{q}_1 \gamma_\mu (1 - \gamma_5) q_2$. The decays with $|V_{cs}V_{ud}| \simeq 1$, $|V_{cq}V_{uq}| \simeq s_c$ and $|V_{cd}V_{us}| \simeq s_c^2$ are classified as the Cabibbo-favored (CF), singly Cabibbo-suppressed (SCS) and doubly Cabibbo-suppressed (DCS) processes, respectively.

By using $\mathcal{H}_{\text{eff}}$ in eq. (2.1), we draw different topological diagrams in $B_c \rightarrow BM$ [32–34], where the quark lines should be in accordance with the operators in eq. (2.2). As seen in figure 1, we obtain six topological diagrams. The external and internal $W$-emission diagrams in figures 1a and b can be parameterized as the topological amplitudes $T$ and $C$, respectively. Since one can factorize $T$ and $C$ as $\mathcal{A} \propto (M|\langle \bar{q}_1 q_2|0\rangle|B_c|\langle \bar{q}_3 c|B_c\rangle) [4]$, which consists of two calculable matrix elements, the $T$ and $C$ are regarded as the factorizable amplitudes [7, 22, 32]. The other internal $W$-emission diagram in figure 1c has no factorizable
form, parameterized as \( C' \). In figures 1(d,e,f), the \( W \)-exchange amplitudes of \((E', E_B, E_M)\) need an additional gluon to relate \( M \) and \( B \). Besides, \( E_B(E_M) \) has the \( W \)-boson to connect \( B \) and \( M \), with the \( c \)-quark transition to be a valence quark in \( B(M) \), whereas \( M \) in the \( E' \) amplitude is unable to connect to the \( W \)-boson. In addition to \( C' \), \((E', E_B, E_M)\) are the non-factorizable amplitudes according to the factorization approach \([32, 35]\). As a result, we clearly identify each (non-)factorizable effect that contribute to the two-body \( B_c \to BM \) decays.

To present the amplitudes of \( B_c \to BM \) with \((T, C)\) and \((C', E', E_B, E_M)\), we need the suitable insertions of the final states to match the quark lines, such as \( \pi^0 = \sqrt{1/2}(u\bar{u} - dd) \), which adds a pre-factor of \( \pm \sqrt{1/2} \) to the topological parameters. Likewise, the \((\eta, \eta')\) meson states that mix with \( \eta_q = \sqrt{1/2}(u\bar{u} + dd) \) and \( \eta_s = s\bar{s} \) lead to the other pre-factors. Specifically, the mixing matrix is presented as \([45]\)

\[
\begin{pmatrix}
\eta \\
\eta'
\end{pmatrix} = 
\begin{pmatrix}
\cos \phi & -\sin \phi \\
\sin \phi & \cos \phi
\end{pmatrix}
\begin{pmatrix}
\eta_q \\
\eta_s
\end{pmatrix},
\]

with the mixing angle \( \phi = (39.3 \pm 1.0)^\circ \). We hence obtain the amplitudes of \( B_c \to BM \), given in table 1. The topological amplitudes are in fact complex, presented as 11 parameters:

\[
T, Ce^{i\delta_C}, C'e^{i\delta_{C'}}, E_B e^{i\delta_{EB}}, E_M e^{i\delta_{EM}}, E' e^{i\delta_{E'}},
\]

(2.4)

with \( T \) set to be relatively real. To obtain the decay widths, we depend on the integration of the phase space for the two-body decays, given by \([43]\)

\[
\Gamma(B_c \to BM) = \frac{|\vec{B}_B|}{8\pi m_{B_c}^2} |A(B_c \to BM)|^2,
\]

\[
|\vec{B}_B| = \sqrt{\frac{m_{B_c}^2 - (m_B + m_M)^2}{m_{B_c}^2 - (m_B - m_M)^2}}.
\]

(2.5)

with \( A(B_c \to BM) \) from table 1.

3 Numerical results

In the numerical analysis, we perform a minimum \( \chi^2 \)-fit, with the equation written as \([25]\)

\[
\chi^2 = \sum_i \left( \frac{B_{th}^i - B_{ex}^i}{\sigma_{ex}^i} \right)^2 + \sum_j \left( \frac{R_{th}^j - R_{ex}^j}{\sigma_{ex}^j} \right)^2,
\]

(3.1)

where \( B (R) \) denotes (the ratios of) the branching ratios. The subscripts \( th \) and \( ex \) stand for the theoretical inputs from the amplitudes in table 1 and the experimental data in table 2, respectively, with \( \sigma_{ex}^i \) the experimental uncertainties. By putting the recent observation of \( B(\Xi_c^0 \to \Xi^- \pi^+) = (1.80 \pm 0.55) \times 10^{-2} \) \([46]\) into \( R_{1,2}(\Xi_c^0) \) in table 2, we determine that \( B(\Xi_c^+ \to \Xi^- K^+) = (5.0 \pm 1.9) \times 10^{-4} \) and \( B(\Xi_c^0 \to \Lambda^0 K^0) = (7.6 \pm 2.6) \times 10^{-3} \). The \( B(\Xi_c^0 \to \Xi^0 \pi^+) \) is extracted from the ratio of \( B(\Xi_c^+ \to \Xi^0 \pi^+)/B(\Xi_c^+ \to \Xi^- \pi^+ \pi^+) = 0.55 \pm 0.16 \) \([43]\)
the CKM matrix elements in the Wolfenstein parameterization, given by [43]

\[ \lambda_2, \lambda_3, \alpha \]

and the newly observed \( B(\Xi^+ \rightarrow \Xi^{-} \pi^+ \pi^+) = (2.86 \pm 1.21 \pm 0.38) \times 10^{-2} \) [49]. We adopt the CKM matrix elements in the Wolfenstein parameterization, given by [43]

\[ (V_{cs}, V_{cd}, V_{us}, V_{ud}) = (1 - \lambda^2/2, 1 - \lambda^2/2, \lambda, -\lambda), \]

with \( \lambda = s_c = 0.22453 \pm 0.00044 \). Subsequently, we fit that

\[ (T, C, C') = (0.41 \pm 0.02, 0.47 \pm 0.08, 0.25 \pm 0.02) \text{ GeV}^3, \]

\[ (E_B, E_M, E') = (0.43 \pm 0.04, 0.14 \pm 0.03, 0.14 \pm 0.07) \text{ GeV}^3, \]

\[ (\delta_C, \delta_{C'}, \delta_{E_B}, \delta_{E_M}, \delta_{E'}) = (31.3 \pm 9.6, 158.1 \pm 5.3, -81.0 \pm 8.8, -32.8 \pm 21.6, -88.0 \pm 1.9) \]

\[ \chi^2 / n.d.f. = 0.5, \]

Table 1. Amplitudes of \( B_c \rightarrow BM \), where \( \lambda_q \equiv V_{cq}V_{uq} \) with \( q = (d, s) \) and \( (s \phi, c \phi) \equiv (\sin \phi, \cos \phi) \) for the \( \eta - \eta' \) mixing.

| Decay modes | Amplitudes/(GeV) |
|-------------|------------------|
| \( \Xi^+ \rightarrow \Sigma^+ K^- \) | \( V_{cS}V_{dS}(E_{d} + E') \) |
| \( \Xi^+ \rightarrow \Sigma^0 K^0 \) | \( V_{cS}V_{dS}(C + C' + E_M + E') \) |
| \( \Xi^+ \rightarrow \Xi^+ K^- \) | \( \lambda_2E_M + \lambda_3E_M \) |
| \( \Xi^+ \rightarrow \Xi^0 K^0 \) | \( \lambda_2(T + E_M) \) |
| \( \Xi^+ \rightarrow \eta K^- \) | \( \lambda_2E_M + \lambda_3(C' + E_M) \) |
| \( \Xi^+ \rightarrow \eta' K^0 \) | \( \lambda_2E_M + \lambda_3(C' + E_M) \) |
| \( \Xi^+ \rightarrow \eta K^+ \) | \( \lambda_2E_M + \lambda_3E_M \) |
| \( \Xi^+ \rightarrow \eta' K^0 \) | \( \lambda_2E_M + \lambda_3(C' + E_M) \) |
| \( \Xi^+ \rightarrow \eta K^0 \) | \( \lambda_2E_M + \lambda_3E_M \) |
| \( \Xi^+ \rightarrow \eta' K^+ \) | \( \lambda_2E_M + \lambda_3E_M \) |
| \( \Xi^+ \rightarrow \eta K^+ \) | \( \lambda_2T + \lambda_3E_M \) |
| \( \Xi^+ \rightarrow \eta' K^0 \) | \( \lambda_2E_M + \lambda_3(C' + E_M) \) |
| \( \Xi^+ \rightarrow \eta K^0 \) | \( \lambda_2E_M + \lambda_3E_M \) |

\[ \lambda_0 = (0.41 \pm 0.02, 0.47 \pm 0.08, 0.25 \pm 0.02) \text{ GeV}^3, \]

\[ \delta_{C}, \delta_{C'}, \delta_{E_B}, \delta_{E_M}, \delta_{E'} = (31.3 \pm 9.6, 158.1 \pm 5.3, -81.0 \pm 8.8, -32.8 \pm 21.6, -88.0 \pm 1.9) \]

\[ \chi^2 / n.d.f. = 0.5, \]
According to the topological diagrams in figure 2, we find that the destructive interference, the number has been reduced to agree with the data. Particularly, as seen in table 1, the contrast, the SU(3) symmetry, the non-factorizable effects can be as significant as the factorizable ones; nonetheless, neglected in the factorization approach. While the theoretical computations show that the non-factorizable effects can be as significant as the factorizable ones; hence, we demonstrate that the diagrammatic approach can explain the data well. Moreover, the non-factorizable effects depicted in figure 1 now show that the non-factorizable effects contribute to the branching ratios of the B_c → BM decays in table 3, together with the recent theoretical results for comparison.

4 Discussions and conclusions

Since χ²/n.d.f = 0.5 presents a good fit, we demonstrate that the diagrammatic approach can explain the data well. Moreover, the non-factorizable effects depicted in figure 1 now show that the non-factorizable effects contribute to the branching ratios of the B_c → BM decays in table 3, together with the recent theoretical results for comparison.

| Branching ratios | Data | (Ratios of) Branching ratios | Data |
|------------------|------|-----------------------------|------|
| 10^2 B(Λ^+_c → p K^0) | 3.16 ± 0.16 [43] | 10^4 B(Λ^+_c → p π^0) | 0.8 ± 1.4 (< 0.27) [3, 48] |
| 10^2 B(Λ^+_c → Λ^0 π^+) | 1.30 ± 0.07 [43] | 10^4 B(Λ^+_c → Λ^0 K^+) | 6.1 ± 1.2 [43] |
| 10^2 B(Λ^+_c → Σ^0 π^+) | 1.29 ± 0.07 [43] | 10^4 B(Λ^+_c → Σ^0 K^+) | 5.2 ± 0.8 [43] |
| 10^2 B(Λ^+_c → Σ^+ π^0) | 1.24 ± 0.10 [43] | 10^4 B(Λ^+_c → pγ) | 12.4 ± 3.0 [43] |
| 10^2 B(Λ^+_c → Ξ^0 K^+) | 0.59 ± 0.09 [1] | 10^2 B(Ξ^0_c → Ξ^− π^+) | 1.80 ± 0.55 [46] |
| 10^2 B(Λ^+_c → Σ^+η) | 0.41 ± 0.20 [47] | R_1(Ξ^0_c) = \frac{B(Ξ^0_c → Ξ^−π^+)}{B(Ξ^0_c → Ξ^0 K^+)} | (0.56 ± 0.12) s^2 | |
| 10^2 B(Λ^+_c → Σ^+η^') | 1.34 ± 0.57 [47] | R_2(Ξ^0_c) = \frac{B(Ξ^0_c → Λ^0 K^0)}{B(Ξ^0_c → Ξ^− π^+)} | 0.42 ± 0.06 [43] |

Table 2. The data for B_c → BM.

with n.d.f = 4 as the number of degrees of freedom, by which we present the branching ratios of the B_c → BM decays in table 3, together with the recent theoretical results for comparison.
By relating the topological diagrams in figure 1 to the symmetry properties of the irreducible forms in the SU(3)\(s\),

\[ B_{c\to BM} \equiv B(B_c \to BM), \]

in comparison with the results from the SU(3)\(f\) symmetry [31, 35] and the calculation with the pole model, current algebra and MIT bag model [32, 35]. The data of \( B(\Xi_c^0 \to \Xi^- K^+, \Lambda^0 K^0) \) are extracted with \( R_{1,2}(\Xi_c^0) \), respectively.

Table 3. The numerical results of the \( B_c \to BM \) decays with \( B_{BM} \equiv B(B_c \to BM) \), in comparison with the results from the SU(3)\(f\) symmetry [31, 35] and the calculation with the pole model, current algebra and MIT bag model [32, 35]. The data of \( B(\Xi_c^0 \to \Xi^- K^+, \Lambda^0 K^0) \) are extracted with \( R_{1,2}(\Xi_c^0) \), respectively.

| \( \Xi_c^0 \) | \( \Lambda \) | \( SU(3)_f \) | Cherng et al. | Our work | Expt. |
|---|---|---|---|---|---|
| \( 10^3 B_{c\to BM} \) | \( 10^3 B_{c\to BM} \) | \( 10^3 B_{c\to BM} \) | \( 10^3 B_{c\to BM} \) | \( 10^3 B_{c\to BM} \) | \( 10^3 B_{c\to BM} \) |
| \( 10^4 B_{c\to BM} \) | \( 10^4 B_{c\to BM} \) | \( 10^4 B_{c\to BM} \) | \( 10^4 B_{c\to BM} \) | \( 10^4 B_{c\to BM} \) | \( 10^4 B_{c\to BM} \) |
| \( 10^5 B_{c\to BM} \) | \( 10^5 B_{c\to BM} \) | \( 10^5 B_{c\to BM} \) | \( 10^5 B_{c\to BM} \) | \( 10^5 B_{c\to BM} \) | \( 10^5 B_{c\to BM} \) |
| \( 10^6 B_{c\to BM} \) | \( 10^6 B_{c\to BM} \) | \( 10^6 B_{c\to BM} \) | \( 10^6 B_{c\to BM} \) | \( 10^6 B_{c\to BM} \) | \( 10^6 B_{c\to BM} \) |

where \( \bar{A}_K \) is reduced as \( \bar{A}_K = V_{cs} V_{as} T \) with \( V_{cs} V_{as} = -V_{cd} V_{ud} \), resulting in \( R_1(\Xi_c^0) \approx (1 + E_B/T)^2 s_c^2 \) with the value of \((0.54 \pm 0.04)s_c^2\) to agree with the data. Indeed, the effects of the SU(3)\(f\) symmetry breaking can give rise to the new parameters added to \( \Xi_c^0 \to \Xi^- K^+ \), instead of \( \Xi_c^0 \to \Xi^- \pi^+ \), such that \( R_1(\Xi_c^0) \) can be fit [25]. Here, our interpretation for \( R_1(\Xi_c^0) \) relies on the additional diagram in figure 2 without invoking the SU(3)\(f\) symmetry breaking.

By relating the topological diagrams in figure 1 to the symmetry properties of the baryon wave functions, such as the (anti-)symmetric quark ordering of \( \Sigma^0(\Lambda^0) \approx (ud \pm du) s \) or the irreducible forms in the SU(3)\(f\) and SU(2) spin symmetries, one can derive the more restrict parameterization of the topological amplitudes [33, 34]. This leads to \( R_1(\Xi_c^0) \approx 1.0s_c^2 \) inconsistent with the data. Moreover, the \( T \) term, which contributes to \( \Lambda_c^+ \to \Sigma^0 M^+ \) with \( M^+ = (\pi^+, K^+) \) in table 1, becomes forbidden in refs. [33, 34]. We hence turn off
the $T$ term in $\Lambda_c^+ \to \Sigma^0 M^+$ as a test fit, and obtain $\chi^2 \sim 30$. Clearly, the more restrict representations cannot explain the data well. Without considering the symmetry properties of the baryon wave functions, our topological amplitudes present the most general forms, which are able to receive the short and long-distance contributions both. The long-distance effect has been proposed in the pole model to contribute to the $W$-exchange process $[32, 35]$. In the $\Xi^0 \to \Xi^- M^+$ decay, $\Xi^0$ transforms as the $\Lambda^0 (\Sigma^0)$ pole followed by the strong decay $\Lambda^0 (\Sigma^0) \to \Xi^- M^+$, which contributes to figures 2 b and c; nonetheless, the latter diagram is forbidden with the more restrict representations. Another example comes from the rescattering effect. With $\Lambda^*$ denoting the higher-wave $\Lambda$ state, the $\Lambda_c^+ \to \Lambda^* \rho^+$ decay has a $T$ amplitude ($T^*$). Through the $\pi^0$ exchange, $\Lambda^* \rho^+$ rescatter into $\Sigma^0 \pi^+$, such that $T^*$ contributes to $T$ in $\Lambda_c^+ \to \Sigma^0 \pi^+$. In fact, the symmetry properties of the meson wave functions are not involved in the $D \to MM$ decays, such that the long-distance contributions have been absorbed into the topological amplitudes $[39, 40, 42, 51]$.

In table 3, the SU(3)$_f$ parameters and topological amplitudes that respect the SU(3)$_f$ symmetry are found to explain the data of $B(\Lambda_c^+ \to BM)$ well, indicating that the SU(3)$_f$ symmetry in $\Lambda_c^+ \to BM$ has no sizeable broken effects. In the $D \to K\bar{K}$ decays, the $W$-exchange processes with $V_{us}V_{ud}$ and $V_{cd}V_{ud}$ are parameterized as $E^{(d)}$ and $E^{(s)}$, respectively. One needs the sizeable broken effect of $|E^{(s)}| > |E^{(d)}|$ to explain $B(D^0 \to K^+ K^-)/B(D^0 \to \pi^+ \pi^-)$ and $B(D^0 \to K^0 \bar{K}^0)$ $[39-42]$. Likewise, since we can present $A(\Xi^0_c \to \Xi^- K^+)$ as $\tilde{A}_K \propto T + \Delta E_B$ with $\Delta E_B \equiv E_B^{(s)} - E_B^{(d)}$, eq. (4.1), whether $\Delta E_B$ is equal to zero or not can be a test of the broken SU(3)$_f$ symmetry. This requires more accurate measurements from BELLEII and LHCb.

We compare the three theoretical results in table 3, which all agree with the observed $B(\Lambda_c^+ \to BM)$. However, the SU(3)$_f$ symmetry gives $B(\Xi^+_c \to \Xi^0 \pi^+)$ at least 2 times smaller than the observation $[31, 35]$. Moreover, the SU(3)$_f$ symmetry and the computations that involve the factorization, pole model, current algebra and MIT bag model present $B(\Xi^+_c \to \Xi^- \pi^+\Xi^- K^+, \Lambda^0 \bar{K}^0)$ with large deviations from the data $[31, 32, 35]$. Since we are able to explain $B(\Xi^+_c \to \Xi^0 \pi^+)$ and $B(\Xi^+_c \to \Xi^- \pi^+, \Xi^- K^+, \Lambda^0 \bar{K}^0)$, the
topological amplitudes are shown to have the advantage to explain the two-body $\Xi_c^0 \rightarrow BM$ decays. To further investigate the $\Xi_c^0 \rightarrow BM$ decays, we present our predictions in table 3. It is worth noting that $E_M$ and $E'$ give a constructive (destructive) interference to $\Xi_c^0 \rightarrow \Sigma^+ K^-(\pi^-)$, such that we obtain $\mathcal{B}(\Xi_c^0 \rightarrow \Sigma^+ K^-) = (22.0 \pm 5.7) \times 10^{-3}$ and $\mathcal{B}(\Xi_c^0 \rightarrow \Sigma^+ \pi^-) = (2.4 \pm 1.5) \times 10^{-4}$, bigger and smaller than the other predictions, respectively. In addition to $\Lambda_c^+ \rightarrow p\pi^0$, there are three singly Cabibbo-suppressed $\Lambda_c^+$ decay modes to be measured. Their branching ratios are predicted as $\mathcal{B}(\Lambda_c^+ \rightarrow n\pi^+, p\eta', \Sigma^+ K^0) = (7.7 \pm 2.0, 7.1 \pm 1.4, 19.1 \pm 4.8) \times 10^{-4}$, where $\mathcal{B}(\Lambda_c^+ \rightarrow n\pi^+)$ is consistent with the value from the SU(3)$_f$ symmetry, whereas $\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ K^0)$ agrees with the theoretical computation in [32, 35].

In summary, we have studied the $B_c \rightarrow BM$ decays within the framework of the diagrammatic approach that respects the SU(3)$_f$ symmetry. With the extraction of the topological amplitudes, we have explicitly presented the two $W$-exchange effects as $E_B$ and $E'$ that contribute to the non-factorizable $\Lambda_c^+ \rightarrow \Xi^0 K^+$ decay, together with the relative phases, where $E_B$ gives the main contribution. We have obtained $\mathcal{B}(\Lambda_c^+ \rightarrow p\pi^0) = (0.8^{+0.9}_{-0.8}) \times 10^{-4}$, which agrees with the experimental upper bound. We have presented that $\mathcal{B}(\Xi_c^+ \rightarrow \Xi^0 \pi^+) = (9.3 \pm 3.6) \times 10^{-3}$, $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+, \Lambda^0 K^0) = (19.3 \pm 2.8, 8.3 \pm 5.0) \times 10^{-2}$ and $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- K^+) = (5.6 \pm 0.8) \times 10^{-4}$ to agree with the data, whereas the other theoretical results have shown sizeable deviations. We have predicted that $\mathcal{B}(\Lambda_c^+ \rightarrow n\pi^+, p\eta', \Sigma^+ K^0) = (7.7 \pm 2.0, 7.1 \pm 1.4, 19.1 \pm 4.8) \times 10^{-4}$, in order to be compared with future BESIII, BELLEII and LHCb measurements.

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