CHEMISTRY AND DYNAMICS IN PRE-PROTOTELLAR CORES

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ABSTRACT

We have compared molecular-line emission to dust continuum emission and modeled molecular lines using Monte Carlo simulations in order to study the depletion of molecules and the ionization fraction in three pre-protostellar cores, L1512, L1544, and L1689B. L1512 is much less dense than L1544 and L1689B, which have similar density structures. L1689B has a different environment from those of L1512 and L1544. We used density and temperature profiles, calculated by modeling dust continuum emission in the submillimeter, for modeling molecular-line profiles. In addition, we have used molecular-line profiles and maps observed in several different molecules toward the three cores. We find a considerable diversity in chemical state among the three cores. The molecules include those sensitive to different timescales of chemical evolution such as CCS, the isotopes of CO and HCO$^+$, DCO$^+$, and N$_2$H$^+$. The CO molecule is significantly depleted in L1512 and L1544 but not in L1689B. CCS may be in the second enhancement of its abundance in L1512 and L1544 because of the significant depletion of CO molecules. N$_2$H$^+$ might already be starting to be depleted in L1512, but it traces very well the distribution of dust emission in L1544. On the other hand, L1689B may be so young that N$_2$H$^+$ has not reached its maximum yet. The ionization fraction has been calculated using H$^{13}$CO$^+$ and DCO$^+$. The result shows that the ionization fraction is similar toward the centers of the three cores. This study suggests that chemical evolution depends on the absolute timescale during which a core stays in a given environment as well as its density structure.

Subject headings: astrochemistry — ISM: clouds — ISM: molecules — radio lines: ISM

1. INTRODUCTION

Many studies have been done on low-mass star formation in detail, theoretically and observationally, over the past two decades. These studies were possible because many low-mass protostellar cores are close, isolated, and geometrically simple. In addition, they evolve slowly, allowing the process to be observed in distinct stages. The information accumulated by these studies now provides the big picture of the evolutionary stages of low-mass star formation. Lada (1987), Myers & Ladd (1993), and André, Ward-Thompson, & Barsony (1993) developed an evolutionary sequence based on the spectral energy distribution (SED) of dust continuum emission through Class 0 to Class III sources, and Adams, Lada, & Shu (1987) supported the evolutionary sequence by modeling the SED theoretically. In addition, several groups (Larson 1969; Penston 1969; Shu 1977; Shu, Adams, & Lizano 1987; Foster & Chevalier 1993; Ciolek & Mouschovias 1994; McLaughlin & Pudritz 1997) have developed dynamical evolution models that theoretically predict different structures of density and velocity in protostellar cores, based on differing initial conditions.

In spite of the big picture of low-mass star formation, the initial collapse is poorly understood. The collapse dynamics and the timescale of evolution are crucially dependent on initial conditions. Pre-protostellar cores (PPCs) are believed to be gravitationally bound, but they have no central hydrostatic protostar (Ward-Thompson, Scott, & André 1994; Ward-Thompson, Motte, & André 1999). Therefore, PPCs can be considered as the potential sites of future star formation and give us the chance to probe the initial conditions of star formation. The series of papers of Ward-Thompson et al. (1994, 1999, 2000; Ward-Thompson, André, & Kirk 2002) and the paper of André, Ward-Thompson, & Motte (1996) argued that the density of PPCs is relatively constant in the inner cores and falls off at larger radii. This is very different from the singular isothermal sphere that leads to “inside-out” collapse (Shu 1977). However, they assumed a uniform temperature in PPCs to calculate density structures. Evans et al. (2001) and Zucconi, Walmsley, & Galli (2001) shows that the temperature of a dust grain decreases toward the centers of PPCs, assuming that dust grains are heated only by the attenuated external radiation field and that the radiation from the core itself is optically thin. Based on their results, Evans et al. (2001) argue that the continuum emission is significantly dependent on the temperature structure as well as the density structure, and they show that Bonnor-Ebert spheres can fit well the submillimeter dust continuum emission in PPCs. In agreement, the recent paper of Ward-Thompson et al. (2002) show that the color temperatures of PPCs that are calculated from the 170 and 200 μm dust emission observed by ISOPHOT decrease toward their centers. As a result of the lower temperature at the center, the density at the center must be more peaked than is the intensity of dust continuum emission. Evans et al. (2001) show that even a power law could fit the density structure of L1544.

Ciolek & Mouschovias (1994) modeled ambipolar diffusion for the quasi-static evolution of a uniformly magnetized isothermal molecular cloud, finding relatively constant...
density toward the center. However, there has been debate about the importance of ambipolar diffusion because of differences between inward velocity observed (Tafalla et al. 1998; Williams et al. 1999) and calculated from the magnetic field (Goodman & Heiles 1994; André et al. 1996; Ward-Thompson et al. 1999, 2000; Crutcher & Troland 2000). These differences might be resolved by calculating more accurate density structure and, in turn, the correct temperature structure from the observed data. Ciolek & Basu (2000) showed that if the density at the center of a PPC were higher, their model could explain the observed magnetic field and inward velocity.

In addition to density and temperature distributions, we need to understand the ionization structure because magnetic relaxation by ambipolar diffusion is tightly related to the ionization structure (Rawlings 2000). The ionization fraction can affect the process of gravitational collapse because the coupling between the ions and magnetic field plays a key role in preventing free-fall collapse of a dense core and slowing the drift of neutral gas through the magnetic field (ambipolar diffusion). In addition, the gas-phase chemical reactions depend significantly on the ionization fraction, and the ionization fraction is highly sensitive to the chemical reactions depend significantly on the ionization fraction can affect the process of gravitational collapse because the coupling between the ions and magnetic field. In addition, the gas-phase chemical reactions depend significantly on the ionization fraction. These theoretical and observational results suggest that the relative distributions of several molecules can be used to probe the timescale of the dynamical evolution of a PPC. However, Rawlings et al. (1992) and Rawlings & Yates (2001) modeled several molecular lines combining self-consistently dynamical, chemical, and radiative transfer models and showed that the abundance variation and the line profiles are very sensitive to the free parameters in the chemical model. Consequently, we need to use multiple transitions and maps in order to constrain these models.

In this paper, we explore the chemical and dynamical differences in three PPCs, L1512, L1544, and L1689B, comparing molecular depletion and ionization fraction by simple analysis of integrated intensity and column density and by modeling several molecular-line profiles in detail. In this study, we cover a very early time molecule (CCS), an early-time molecule (CO), a middle-time molecule (HCO$^+$), and a very late time molecule (N$^+_2$H$^+$) in chemical evolution. According to the chemical models of Bergin & Langer (1997) and Aikawa et al. (2001), which used an initial density of $10^4$ cm$^{-3}$, the CCS abundance decreases rapidly after a few $\times 10^4$ yr since CCS is a polar molecule and it is easily frozen out onto the surface of dust grains. In addition, CCS is destroyed by HCO$^+$ or H$_2$O$^+$, whose abundances increase until about $10^6$ yr. Even though CO is a nonpolar molecule, it has very high binding energy ($1740$ K onto water ice mantle grains; Bergin & Langer 1997). As a result, CO starts to be depleted onto the surface of dust grains after about $10^6$ yr, causing the depletion of HCO$^+$ in turn. HCO$^+$ is formed by the interaction between H$_3^+$ and CO or H$_2$D$^+$ and CO. However, N$_2$, which is the precursor of N$_2$H$^+$, starts to be abundant much later than other molecules and reaches its maximum around $10^7$ yr. N$_2$ has a low binding energy ($750$ K; Aikawa et al. 2001) onto the surface of dust grains, so it is not frozen out from the gas phase easily. In addition, H$_3^+$, which is the other precursor of N$_2$H$^+$, increases as CO is depleted. Another cause of the enhancement of N$_2$H$^+$ at late times is the decline of the destruction of N$_2$H$^+$ by CO, which is significantly depleted at late times.

We observed multiple positions in each core to study the chemical distribution within a core, in addition to studying the chemical differences among the three PPCs. The most important aspect of this study is that we start with reasonable physical models calculated from dust analysis. The density and temperature structures found by Evans et al. (2001) are adopted for modeling molecular-line profiles.

In § 2 we summarize observational parameters, and § 3 shows the results of observations. In § 4 we analyze the column densities of several molecules. Section 5 compares modeled molecular-line profiles and observed line profiles. Finally, we discuss our results regarding depletion and ionization in the view of chemical and dynamical evolution in § 6.

2. OBSERVATION

We observed the three PPCs in C$^{18}$O $J = 2-1$ and $J = 3-2$, C$^{17}$O $J = 2-1$, DCO$^+ J = 3-2$, HCO$^+ J = 3-2$, and H$^{13}$CO$^+ J = 3-2$ with the 10.4 m telescope of the Caltech Submillimeter Observatory (CSO) at Mauna Kea, Hawaii, from 1995 to 2002. We used an SIS receiver with an acousto-optic spectrometer (AOS) with a 50 MHz bandwidth and 1024 channels, and the frequency resolution was about 2–2.5 channels, 0.13–0.16 km s$^{-1}$ at around 220 GHz. The pointing uncertainty was about 4" on average. We also observed these cores in H$^{13}$CO$^+ J = 1-0$, N$_2$H$^+ J = 1-0$, and CCS $N_J = 4_1-3_2$ with the 45 m telescope of the Nobeyama Radio Observatory in Japan in 2002 January. We used the S40, S80, and S100 receivers with an AOS with a 40 MHz bandwidth and 2048 channels. The frequency resolution was about 2 channels (about 40 kHz), so that the velocity resolution was about 0.27, 0.14, and 0.13 km s$^{-1}$ at 43, 86, and 100 GHz, respectively. The observed sources are listed in Table 1; the observed lines and the main-beam efficiency ($\eta_{\text{mb}}$) of each observation are summarized in Table 2. In Table 1, the last column shows the offsets of the dust peaks from the given coordinates; all offsets in figures other than Figures 2 and 3 are relative to the dust peak, assumed to be the center of the core in all modeling.
3. RESULTS

3.1. Spectra

Figure 1 shows the spectra of molecular lines observed toward the centers of the three PPCs. The centers are the positions of the centroids of the dust emission (Shirley et al. 2000). Most of the molecular lines have not been mapped completely but observed through two orthogonal cuts in $\alpha$-$\delta$, crossing at the centers of dust emission in the cores. We do not see any consistent trend in the intensity of each spectrum from core to core. For example, the $^{13}$CO and $^{12}$CO lines are the strongest in L1689B, but $N_2H^+$ and CCS are the strongest in L1544. All the lines except for $N_2H^+$ and CCS are much weaker in L1512 than in L1689B. The line width (FWHM) of the $^{13}$CO $J = 2$–1 line is about 0.3, 0.5, and 0.6 km s$^{-1}$ in L1512, L1544, and L1689B, respectively.

3.2. Maps

Figure 2 shows maps of three PPCs, in which the gray scale indicates 850 $\mu$m dust continuum intensity and the contours are for the integrated intensities of the $^{13}$CO $J = 2$–1 and DCO$^+ J = 3$–2 lines. We can see that the peaks of dust emission and $^{13}$CO $J = 2$–1 emission are not consistent. In the map for L1512 especially, the centroid of the dust emission coincides with a hole in the $^{13}$CO $J = 2$–1 emission. In contrast, the distribution of the DCO$^+ J = 3$–2 emission appears to peak toward the center of dust emission in L1544 and L1689B, even though our maps of the DCO$^+ J = 3$–2 emission are not complete.

4. SIMPLE ANALYSIS

In this section, we use a simple analysis with standard techniques for comparison to similar work done by others, and in the next section, we deal with detailed models. We use dust emission as the tracer of column density least affected by chemistry in this section, and we assume that the dust emissivities do not change with radius. If temperature decreases toward the center, the column density calculated from dust emission with the assumption of an isothermal case could be underestimated toward the center. Even though the absolute column density calculated from the dust emission can change with the assumed dust opacity by a factor of 2 or 3, its relative distribution with radius can be traced relatively well by dust emission.

4.1. Integrated Intensities

We can compare the distribution of a molecular component with that of the dust component within a core using the integrated intensity of an optically thin molecular line and the dust continuum intensity observed at a submillimeter wavelength. In the top panels of Figure 3, we plot the logarithmic integrated intensities of the CCS $N_J = 4_3$–$3_2$, $H^{13}$CO$^+$ $J = 1$–0, and $N_2H^+$ $J = 1$–0 lines in order to compare to the 850 $\mu$m dust continuum intensity through the cuts with constant declination shown in Figure 2. The dust continuum intensity and the $H^{13}$CO$^+$ intensity have been shifted upward to compare the shapes of intensity distributions with radius more effectively, and the intensity of dust continuum has been measured into apertures of 20$''$, spaced by 20$''$ for consistency with the $H^{13}$CO$^+$ and $N_2H^+$ observations.

| Molecule | Transition | Frequency (MHz) | Beam Width (arcsec) | Velocity Resolution (km s$^{-1}$) | $T_{MB}^a$ (L1512/L1544/L1689B) |
|----------|------------|----------------|---------------------|-----------------------------|-------------------------------|
| $^{13}$CO | $J = 2$–1$^b$ | 224714.385 | 33 | 0.17 | 0.65/0.65/0.80 |
| $^{13}$CO | $J = 1$–0$^b$ | 219560.357 | 34 | 0.15 | 0.69/0.66/0.60 |
| $^{13}$CO | $J = 3$–2$^a$ | 329350.507 | 26 | 0.10 | 0.59/0.59/0.63 |
| HCO$^+$ | $J = 1$–0$^d$ | 267557.620 | 26 | 0.15 | 0.49/0.66/0.65 |
| HCO$^+$ | $J = 3$–2$^{a,c}$ | 86754.330 | 18 | 0.14 | 0.49/0.49/0.49 |
| HCO$^+$ | $J = 2$–1$^{a,c}$ | 260255.617 | 26 | 0.16 | None/0.49/0.65 |
| DCO$^+$ | $J = 3$–2$^b$ | 216112.605 | 35 | 0.15 | 0.65/0.69/0.60 |
| CCS | $N_J = 4_3$–$3_2$ | 45379.033 | 37 | 0.27 | 0.77/0.77/0.77 |
| $N_2H^+$ | $J = 1$–0$^d$ | 93173.809 | 17 | 0.13 | 0.50/0.50/0.50 |

$^a$ The term $T_{MB} = T_A^d/T_R^d$, where $T_A^d$ is the radiation temperature and $T_R^d = T_R^d$ only if a source fills the beam (Kutner & Ulrich 1981).
$^b$ Observed with CSO 10.4 m telescope.
$^c$ Gregersen & Evans 2000.
$^d$ Observed with Nobeyama 45 m telescope.
The dust emission of L1512 is about half that of L1544, and the distribution is not as peaked as that of L1544 and L1689B. L1544 and L1689B have similar dust emission, even though it is more peaked in L1544. However, the CCS intensity of L1689B is more similar to that of L1512 than to that of L1544, and the CCS intensity of L1544 is about twice those in L1512 and L1689B. The CCS intensity in all three PPCs is not peaked as much toward the center as the dust emission. However, it has a bump toward the centers of L1512 and L1544 (see § 6.1). In L1689B, the bump is not certain because of the low signal-to-noise ratio (S/N).

If we check the relative variations of the integrated intensity of the $^{13}$CO $J = 1-0$ line with radius in each core, in L1689B it is skewed to the west but follows well the dust continuum emission, decreasing at the edge of the core. On the other hand, the distribution of the integrated intensity of the $^{13}$CO $J = 1-0$ line in L1512 is not well matched with dust continuum, and the integrated intensity is even depressed toward the center. We also see the depression of $^{13}$CO$^+$ emission at the center of L1544. This depression was predicted by Caselli et al. (2002) in their chemical models but not observed, probably because their angular resolution (28") was worse than ours (18"). We suspect that the optical depth of the $^{13}$CO$^+$ $J = 1-0$ line in L1544 and L1689B is not negligible. Therefore, the depression in those cores could be partially caused by optical depth. However, L1689B does not show a depression even though it has a density structure similar to L1544, suggesting that depletion is playing a major role in L1544.

The N$_2$H$^+$ intensity is well peaked in L1544 and shows almost the same shape as the dust emission. L1689B also shows similar shapes in dust emission and N$_2$H$^+$ intensity. However, the N$_2$H$^+$ intensity of L1689B is only two-thirds of that of L1544, even though these two cores have very similar dust emission and density structures, with central densities of $10^6$ cm$^{-3}$. In L1689B, the peak of the intensity of N$_2$H$^+$ is shifted from that of the intensity of the dust emission similarly to the intensity of $^{13}$CO$^+$. However, the ratio of the intensity of $^{13}$CO$^+$ to the intensity of N$_2$H$^+$ at

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**Fig. 1.**—Observed spectra toward the dust peaks of the three PPCs. The dotted line in the panels of the third row shows the results of fitting the hyperfine structure of C$^{17}$O $J = 2-1$ line profiles using solutions in CLASS.
the center of L1689B is greater than that in the other two cores.

In L1512, with a central density of $10^5$ cm$^{-3}$, $N_2H^+$ emission is more extended than the dust, unlike in the other cores. Since the optical depth of the $N_2H^+$ $J = 1-0$ line in L1512 is smaller than in L1544 (Benson et al. 1998), this might indicate the possible presence of depletion at the dust peak.

In the following section, we compare the distributions of the CO isotopes to the distribution of dust emission by using molecular hydrogen column densities calculated from them instead of using the intensity distribution, because the optical depth effect in the $^{13}$CO line can be calculated and the standard abundance of CO is known.

4.2. Column Density

We compare the $H_2$ column densities calculated from observed molecular-line intensities with those calculated from submillimeter continuum emission. This simple analysis assumes the following: (1) dust continuum emission traces all material along a line of sight in a core, and dust and gas are well mixed; (2) the core is isothermal, and dust and gas are well coupled, so that they have the same temperature; (3) molecular abundances are constant through the
core; and (4) all levels are in LTE. Therefore, the excitation temperatures in all levels are the same as the kinetic temperature and the same as the dust temperature.

4.2.1. The H$_2$ Column Density from Molecular Emission Lines

If we assume a line is very optically thin so that absorption can be completely neglected, the equation of radiative transfer is given by

$$\frac{dI_{\nu}}{ds} = -\frac{h\nu_{ul}A_{ul}}{4\pi} n_u,$$

where $n_u$ is the number density of the upper level and $A_{ul}$ is the Einstein coefficient. For the transition $J \rightarrow J-1$ in a linear molecule, the resulting relation between $N(x)$, the column density of molecule $x$, and the integrated intensity of the line is

$$N(x) = \frac{3kQe^{E_J/kT_{ex}}}{8\pi^3\mu_l^2J} \int T_R dv,$$

where $E_J = hBJ(J+1)$, $B$ is the rotational constant, $T_{ex}$ is the excitation temperature above the ground state, $\mu$ is the dipole moment, and $Q$ is the partition function. Equation (2) is valid only in the limit that $\tau \rightarrow 0$. For finite optical depth, an optical depth correction can be applied:

$$N_{\text{thick}} = N_{\text{thin}} \frac{\tau_{\nu}}{1 - e^{-\tau_{\nu}}}. \tag{3}$$

In principle, one should also correct for the presence of the cosmic background radiation, $T_{\text{CMB}}$, but for the lines considered here, at $\lambda < 1.4$ mm, the Planck function in temperature units is less than 0.23 K, completely negligible compared to likely values of $T_{\text{ex}}$. The effect on $N(x)$ of neglecting $T_{\text{CMB}}$ is less than 5% for $T_{\text{ex}} \geq 10$ K and $\tau \leq 1$, typical of the conditions relevant here. These effects are less than any plausible calibration uncertainty.

The rotational constant and the dipole moment of each molecule used for this calculation are listed in Table 3. For

![Diagram](image-url)

**FIG. 3.**—Top: Comparison of the integrated intensities of the CCS $N_J = 4-3$, H$^{13}$CO$^+$ $J = 1-0$, and N$_2$H$^+$ $J = 1-0$ lines with $S_{850}$ through the cuts marked in Fig. 2. Here $S_{850}$ is shifted by 0.9, and $I_{H^{13}CO^+}$ is shifted by 0.4 in the logarithmic scale. Bottom: Comparison of the column densities of hydrogen molecules calculated from the $850 \mu$m dust continuum emission, C$^{18}$O $J = 2-1$ line (without the correction of $\tau$), and C$^{17}$O $J = 2-1$ line (with correction of $\tau$) through the cuts marked in Fig. 2. The errors in molecular intensities account only for the rms noises of spectra, so that the error bars show the minimum errors. In $N(H_2)$ derived from the C$^{18}$O of L1544 and L1689B, the error in fitting the hyperfine structure is also included.

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| Isotope       | Rotational Constant $B$ (MHz) | Dipole Moment $\mu$ (D) | Abundance $X (= n_i/n_{H_2})$ |
|---------------|-------------------------------|-------------------------|-------------------------------|
| C$^{18}$O     | 54891.423                     | 0.11079                 | $4.8 \times 10^{-7}$          |
| C$^{17}$O     | 56179.982                     | 0.11034                 | $1.5 \times 10^{-7}$          |
the excitation temperature, we used the kinetic temperature of 10 K, a typical value in dark molecular clouds, under the assumption that all lines are thermalized; that is, \( T_l = T_{\text{ex}} = T_k = 10 \) K. If we use 20 K for this calculation, the result is changed only by a factor of 1.2 for the \( J = 2-1 \) line of C\(^{18}\)O and C\(^{17}\)O.

We calculated the column densities using the C\(^{18}\)O \( J = 2-1 \) and C\(^{17}\)O \( J = 2-1 \) lines. First, the lines were assumed to be optically thin. However, we can calculate the optical depth of the C\(^{18}\)O \( J = 2-1 \) line directly by comparing the relative intensities of its nine hyperfine components (Ladd, Fuller, & Deane 1998). The optical depth of the C\(^{17}\)O \( J = 2-1 \) line was obtained by fitting a method in the program CLASS. The panels in the third row of Figure 1 show the results of fitting the hyperfine components of the C\(^{17}\)O \( J = 2-1 \) line in the center of each core. The total optical depths for L1544 and L1689B are not small enough to be ignored (Table 4), even though each individual hyperfine component is optically thin. In order to correct for this optical depth effect, we applied equation (3) to the above calculation for an optically thin line. For the C\(^{18}\)O \( J = 2-1 \) line, \( \tau_v \) is the optical depth of the line center, which is calculated by multiplying the relative strength (0.693) of the main group, which has four close components, by the total optical depth. The correction factors at the centers of L1544 and L1689B are about 1.4. Note that we do not use the excitation temperature of C\(^{18}\)O \( J = 2-1 \) obtained by fitting the hyperfine structure to calculate the column density of C\(^{18}\)O because this method assumes that \( T_{\text{ex}} \) is constant along the line of sight. Our detailed models (see § 5.1) show that this assumption leads to incorrect results. In addition, we want to use the same method for C\(^{17}\)O and C\(^{18}\)O and compare the results.

Finally, we convert the column density of each molecule into the H\(_2\) column density using the abundance \( \chi \) of molecule \( x \):

\[
N(H_2) = \frac{N(x)}{\chi(x)} \text{ cm}^{-2}.
\]

We used a CO abundance of 2.7 \( \times \) 10\(^{-4}\) (Lacy et al. 1994), about 3 times greater than the abundance used in other studies, such as Bachmann et al. (2002) and Jorgensen, Schoier, & van Dishoeck (2002). The abundance ratios [CO/C\(^{18}\)O] and [C\(^{18}\)O/C\(^{17}\)O] are about 560 \( \pm \) 25 and 3.2 \( \pm \) 0.2, respectively (Wilson & Rood 1994). The abundance of each molecule used in calculating the H\(_2\) column density is listed in Table 3.

### 4.2.2. The H\(_2\) Column Density from Dust Continuum Emission

If the emission from dust is optically thin, the observed flux density \( S_d \) can be related to the column density of gas by

\[
N(H_2) = \frac{S_d}{\mu m_H \kappa_d B_\nu(T_d) \Omega}.
\]

where \( \mu \) is the mean molecular weight, \( m_H \) is the atomic mass unit, \( \kappa_d \) is the mass opacity of dust per gram of gas, \( B_\nu \) is the Planck function, and \( \Omega \) is the aperture solid angle; \( \Omega = (\pi \theta^2) / (4 \ln 2) \) for a circular Gaussian aperture.

We use column (5) of the Ossenkopf-Henning dust opacity table (Ossenkopf & Henning 1994), which represents agglomerated dust grains with thin ice mantles, and assume a gas-to-dust mass ratio of 100 to get \( \kappa_{850} = 0.018 \text{ cm}^{-2} \text{ g}^{-1} \). We use the 850 \( \mu \)m data from Shirley et al. (2000) but measure the flux in an aperture of 33\(^\circ\), the size of main beam in the observations of C\(^{17}\)O. If the dust temperature \( T_d \) is 10 K, the H\(_2\) column density can be calculated from

\[
N(H_2) = 3.36 \times 10^{22} S_{850} \text{ (Jy cm}^{-2} \text{ )}.
\]

If the temperature were 20 K, the calculated \( N(H_2) \) would be lower by a factor of 3.3.

#### 4.2.3. Results

The C\(^{18}\)O \( J = 2-1 \) and C\(^{17}\)O \( J = 2-1 \) lines have been used to calculate the H\(_2\) column density assuming constant molecular abundances. Basically, we assume the lines are optically thin. If a molecular line is optically thick, then the calculation with equations (2) and (4) underestimates the H\(_2\) column density. As mentioned in the previous section, however, we can calculate the optical depth of the C\(^{18}\)O \( J = 2-1 \) line by fitting its hyperfine structure. We have corrected the column density of the C\(^{17}\)O \( J = 2-1 \) line for optical depth in L1544 and L1689B even though the correction is not very big.

The results of fitting the hyperfine components of C\(^{17}\)O \( J = 2-1 \) show that the total optical depth of this line is about 0.1 in L1512, but it is negligible at the central positions in L1544 (\( \tau \approx 1.0 \)) and L1689B (\( \tau \approx 0.8 \)). In L1512, the error of the calculated optical depth is very big, because of the low S/N in the weak components. However, the ratio (\( \approx 4.3 \)) between the strongest component and the second-strongest component in L1512 is bigger than that (\( \approx 3.3 \)) in the two other cores, so the total optical depth would be less than that of L1689B, at least. The abundance of C\(^{18}\)O is about 3.2 times greater than that of C\(^{17}\)O. Therefore, the optical depth of C\(^{18}\)O is about 3.2 greater than the total optical depth of C\(^{17}\)O, and the optical depth of C\(^{18}\)O \( J = 2-1 \) must be considered in calculating column densities. We plot the H\(_2\) column density calculated from the C\(^{17}\)O \( J = 2-1 \) line in the bottom panels of Figure 3, where the optical depth effect has been corrected by equation (3). However, in the figure, we use the H\(_2\) column density calculated from the C\(^{18}\)O \( J = 2-1 \) line based on the optically thin line approximation without correcting for its optical depth in order to show the significance of the optical depth effect. In fact, C\(^{17}\)O has been observed in fewer positions, so we cannot calculate the optical depth of every C\(^{18}\)O spectrum.

In the figure, we see significant differences between the H\(_2\) column densities calculated from the 850 \( \mu \)m emission and the C\(^{18}\)O \( J = 2-1 \) line in all three PPCs. At central positions, the H\(_2\) column density calculated from the C\(^{18}\)O \( J = 2-1 \) line is about 15 times smaller in L1512 and L1544 and 8 times smaller in L1689B than the H\(_2\) column densities calculated from the 850 \( \mu \)m emission. However, after correcting

### TABLE 4

| Source     | Total Optical Depth |
|------------|---------------------|
| L1512      | 0.10 \( \pm \) 2.17 |
| L1544      | 1.03 \( \pm \) 0.42 |
| L1689B     | 0.79 \( \pm \) 0.24 |
for the optical depth of the C$^{17}$O $J = 2$–1 line, the difference between the H$_2$ column densities calculated from S$_{850}$ and from C$^{18}$O has been reduced. In L1689B especially, the difference is just a factor of 2 after the correction.

Another interesting thing is that the distribution of C$^{13}$O in L1544 does not show the central depression observed in Caselli et al. (1999). This is probably due to the larger beam (33") in this observation compared to that (21") of Caselli et al. (1999), similar to the case of H$^{13}$CO$^+$ (see § 4.1). This result suggests that inadequate resolution can prevent us from calculating the actual depletion of the molecules.

### 4.3. Conclusions

The integrated intensities and the H$_2$ column densities calculated from several molecules have been compared with the intensity of 850 $\mu$m dust emission and the H$_2$ column densities calculated from the dust emission in our simple analysis of molecular-line observations. The first result of this analysis is that the dust emission is more peaked than the molecular emission. The depression of molecular emission toward the centers is partially caused by the optical depth effect on molecular lines. We can see this effect comparing the column densities calculated from the C$^{18}$O $J = 2$–1 (marginally optically thin and corrected by $\tau$) and C$^{13}$O $J = 2$–1 (optically thick but not corrected by $\tau$) lines. The correction for the optical depth effect by the C$^{18}$O $J = 2$–1 line removes some of the difference between the H$_2$ column densities calculated from the C$^{18}$O $J = 2$–1 line and dust emission. The remaining considerable discrepancy would be caused by the depletion of CO molecules. This result shows that we can overestimate the depletion of a molecule if we use an optically thick line without correcting for the optical depth. Jørgensen et al. (2002) have compared the H$_2$ column densities calculated from the 1.3 mm dust continuum and the C$^{17}$O (1–0) line and found similar depletion factors of CO to ours in L1544 and L1689B. Redman et al. (2002) also used the same analysis of C$^{17}$O $J = 2$–1 and 850 $\mu$m dust emission toward L1689B to show a result similar to ours. We explore the depletion in detail through modeling molecular-line profiles using the Monte Carlo (MC) method in the next section. We emphasize that the amount of the discrepancy varies from core to core. After the correction for the optical depth effect, the H$_2$ column density calculated from the C$^{18}$O $J = 2$–1 line is 11 times smaller in L1512, 9 times smaller in L1544, and 2 times smaller in L1689B than the H$_2$ column density calculated from dust emission (Table 5).

The simple method used in this analysis clearly reveals evidence for depletion, but it has several limitations for quantitative analysis. First, the beam size of each line observation is not the same. If we had mapped these cores completely in each line, then we would have been able to convolve the maps using the same beam size. Second, the variations of the excitation temperature and the abundance of a molecule along the line of sight are not included in this simple analysis. In addition, the absolute H$_2$ column density calculated from dust emission may be uncertain by a factor of 2–3 because of the uncertainty of dust opacity. Because of these limitations, we have to model molecular lines and compare them to the observed lines in order to study depletion in more detail.

### 5. Detailed Models

#### 5.1. Method

We use the MC method to calculate the radiative transfer of molecular lines (Bernes 1979; Choi et al. 1995). The MC code for this work has been developed by Choi et al. (1995). The MC code generates model photons at a random position, in a random direction, and at a random frequency with proper random number distributions. These photons go through a one-dimensional spherically symmetric molecular cloud adjusting the level populations of molecules. The MC code calculates the excitation by the model photons and uses statistical equilibrium to adjust each level population until the criteria of convergence are satisfied. The MC method is more powerful than the large velocity gradient method because it can deal with arbitrary distributions of systematic velocity, density, kinetic temperature, microturbulence, and abundance self-consistently. Therefore, we can combine reasonable physical models from analysis of dust emission with chemical models to produce molecular-line simulations, and the depletion of molecules with radius can be tested.

For the MC simulation, we need collision rates at lower gas temperatures than are usually available, so we extrapolate linearly to 5 K the collision rates for CO (Flower & Launay 1985), which we use for C$^{18}$O and C$^{17}$O. Similarly, we extrapolate the downward collision rates for HCO$^+$ (Flower 1999) to use for H$^{13}$CO$^+$ and DCO$^+$. Upward rates are calculated for detailed balance for each isotope. The size of each core is fixed at 0.15 pc, and microturbulent velocity is assumed constant through each modeled core.

Once the MC code calculates each level population, we simulate specific molecular-line profiles using the virtual telescope simulation to compare the modeled profiles with observed molecular-line profiles. We can simulate a molecule with multiple transitions and multiple positions simultaneously in a specific core with the parameters such as beam sizes and main-beam efficiencies that we used in the actual observations. The remaining lack of realism is caused by geometric differences between a one-dimensional simulation and the actual core. As seen in Figure 2, the three cores are not perfectly spherically symmetric but instead are elongated. In order to compare simulated line profiles with real observations, we averaged the lines that have been observed at the same distance from the centers, e.g., the lines in the off-positions of $\pm 30''$ in $\alpha$ and $\delta$. However, some lines have not been averaged in all four directions because the observation did not cover all parts. We need to map cores fully and use a two-dimensional code to do more accurate comparisons.

We model the transitions of four molecules, C$^{18}$O ($J = 2$–1 and $J = 3$–2), DCO$^+$ ($J = 3$–2), H$^{13}$CO$^+$ ($J = 1$–0 and $J = 3$–2), and HCO$^+$ ($J = 3$–2). If the gas and
the density structure is compared to that of the best fitting (1998) and Williams et al. (1999) in L1544. The resulting gas. However, for a density lower than about $10^4$ cm$^{-3}$, the dust of a core are well mixed and well coupled, we can apply the density to the gas. However, for a density lower than about $10^4$ cm$^{-3}$, the gas temperature is not coupled well with the dust temperature. The excitation temperatures of the lines that have high critical density such as DCO$^+$ and H$^{13}$CO$^+$ are mainly dependent on density, so that the inner, denser region mainly contributes to the intensities of those molecular lines, and the outer, less dense region does not change our results much. However, we should in principle correct for the difference between gas and dust temperatures in the outer, less dense parts of cores, especially for the molecular lines such as C$^{18}$O lines that have low critical density. We leave this correction for a future work.

5.2. Physical Models

We use two different types of physical models: Bonnor-Ebert spheres (Bonnor 1956; Ebert 1955) and Plummer-like models (Whitworth & Ward-Thompson 2001). Both these models allow an initial density distribution that is nearly constant for small radii but approaches a power law at large radii. The Bonnor-Ebert sphere provides a good fit to the dust continuum emission of the three PPCs that we are modeling (Evans et al. 2001). The Plummer-like model can fit the dust continuum data for L1544 (Whitworth & Ward-Thompson 2001). It has the advantage that it provides a simple solution for the density and velocity field during a free-fall collapse from the initial state, thereby providing a velocity field, which we need for modeling some of our lines. The initial radial density profile (Whitworth & Ward-Thompson 2001) is

$$\rho(r, t = 0) = \rho_{\text{flat}} \left[ \frac{R_{\text{flat}}}{(R_{\text{flat}}^2 + r^2)^{3/2}} \right]^{\eta}. \quad (7)$$

Even though this model is very simple, in that it assumes a pressure-free collapse, it may be able to explain the later phase of the evolution of PPCs. Li et al. (2002) show that the evolution of a core driven by ambipolar diffusion comes closer to the evolution of a nonmagnetic, free-falling core at higher density.

We use the Bonnor-Ebert sphere model that best fits the dust emission (Evans et al. 2001), and we assume a purely microturbulent velocity field, except for the HCO$^+$ $J = 3 \rightarrow 2$ lines in L1544 and L1689B and the H$^{13}$CO$^+$ lines in L1544. Because those line profiles show deep self-absorption features indicative of systematic radial velocities, we use a Plummer-like model for them. To constrain the various parameters in the Plummer-like model, we model the dust emission, as was done by Evans et al. (2001). The resulting values that best fit the data for both L1689B and L1544 are as follows: $\eta = 3$, the initial $\rho_{\text{flat}} (t = 0)$ of $5 \times 10^3$ cm$^{-3}$, and $R_{\text{flat}} = 2800$ AU. Whitworth & Ward-Thompson found a steeper density structure ($\eta = 4$) and a greater $R_{\text{flat}} (5350$ AU) because they used an isothermal sphere for their model. When the temperature decline toward the center is included, a smaller $R_{\text{flat}}$ is needed. The evolutionary timescale that fits the dust emission well is half the timescale at which the central point mass is formed (the start of the Class 0 stage). The maximum velocity in this model is about 0.08 km s$^{-1}$, which is consistent with the results of Tafalla et al. (1998) and Williams et al. (1999) in L1544. The resulting density structure is compared to that of the best fitting Bonnor-Ebert sphere in Figure 4a; they are very similar. Likewise, the resulting dust temperature structure is very similar (Fig. 4b). The velocity field from the Plummer-like model is shown in Figure 4c.

While the density and temperature structure of the best-fitting Plummer-like model is very similar to that of the best-fitting Bonnor-Ebert sphere, the former does contain a systematic velocity field. To check whether that field affected the results for lines modeled with the Bonnor-Ebert sphere, we model all other lines using the Plummer-like model. The velocity structure does not affect the line profiles of C$^{18}$O, DCO$^+$, and H$^{13}$CO$^+$; the two models give the same results.

5.3. Results of Models

The main purpose of this modeling is to find how much a specific molecule is depleted, and how the depletion is distributed with radius, by simulating molecular-line profiles at multiple positions within a core and by comparing the simulated line profiles with observed line profiles. We tried several functional forms, such as exponential, power-law, Plummer-like, and step functions, for the distribution of a molecular abundance. In addition, we applied the results of Li et al.’s (2002) dynamical and chemical model to our modeling, but their model has too high a systematic velocity to fit the observed molecular-line profiles. However, the group is improving their chemical and dynamical models while communicating with us. Figure 5 and Table 6 show the comparison between results of different functional forms of depletion with radius in the C$^{18}$O (2–1) line simulations. We used integrated temperatures to calculate $\chi^2$ in each model. Among those distributions, a step functional distribution best fits the observed line profiles with radius. This seems reasonable because the results of the chemical models show a sharp decrease in abundance with density or time. Here we mainly show the results of the modeling with the abundance distribution of a step function that has three free parame-
The undepleted abundance of a molecule \( X_0 \), the fractional depletion \( f_D = X/X_0 \), and the radius inside which a molecule is depleted \( r_D \). Each can be different in different species. Therefore, the total depletion of a molecule is dependent on the combination of \( f_D \) and \( r_D \). We emphasize that the derived depletion factor from this modeling has an uncertainty of about a factor of 3 because of the uncertainty of the density structure calculated from the dust analysis.

We compare the distributions of observed and modeled integrated temperatures with radius to find the best fits. Figure 6a shows the distribution of the reduced \( \chi^2 \) of the models in the \( \text{C}^{18}\text{O} \) (2–1) and (3–2) lines of L1512 in the space of \( f_D \) and \( r_D \). The depletion radius is well constrained around 0.075 pc, but the fractional depletion is constrained only to be greater than about 25. This trend occurs in every molecule that is significantly depleted, so we consider \( f_D \) to be the lower limit of the depletion factor. In other words, the data are consistent with complete depletion inside some \( r_D \). However, the distribution of \( \chi^2 \) constrains only the upper limit of the depletion radius in \( \text{H}^{13}\text{CO}^+ \) and \( \text{DCO}^+ \) of L1689B and in \( \text{DCO}^+ \) of L1544, which show small \( r_D \) and \( f_D \) (see Tables 8 and 9). For example, the \( \chi^2 \) in \( \text{H}^{13}\text{CO}^+ \) of L1689B changes within a factor of about 2 (from 3 to 7) in all ranges of \( f_D \) within \( r_D < 0.011 \) (Fig. 6b). As we men-

### TABLE 6

| Function                  | \( X \)                  | \( \chi^2 \) |
|---------------------------|--------------------------|--------------|
| Step……..\( X_0 \) & \( r < 0.045 \text{ pc} \) | 10            |
| Plummer-like…………………\( X_0 \left( \frac{r}{\sqrt{r^2 + (0.05)^2}} \right)^2 \) | 76            |
| Power law………………….\( X_0 \left( \frac{r}{0.15} \right)^{1.7} \) | 117           |
| Exponential………………..\( X_0 \exp\left( -\frac{0.04}{r} \right) \) | 93            |

\( X_0 = 4.82 \times 10^{-7} \).
tioned above, the density structure has an uncertainty of a factor of about 3, so the calculated depletion in this model could have the same uncertainty.

5.3.1. C$^{18}$O J = 2–1 and J = 3–2

The best fits of the C$^{18}$O J = 2–1 and J = 3–2 line profiles in the three cores are shown in Figure 7. The parameters of the best-fit models are summarized in Table 7. We use the standard C$^{18}$O abundance of 4.82 × 10$^{-7}$ for the undepleted abundance ($X_0$) for all cores, which was used to calculate the column density of H$_2$ (§ 4.2.1). According to the results, CO molecules are depleted within 0.075 pc (about 110$''$) by a factor of 25 in L1512, so CO is depleted everywhere in our C$^{18}$O map. In the case of L1544, the depletion factor is 25 within 0.045 pc (about 70$''$). The C$^{18}$O J = 2–1 and J = 3–2 line profiles simulated simultaneously at different positions from the center fit the observed line profiles well in L1512 and L1544. On the other hand, we do not find a model to fit well all the observed line profiles from the center to the off-position of 90$''$ in L1689B. The antenna temperatures of the observed J = 2–1 and J = 3–2 lines are almost the same or increase outward from the center in L1689B, even though the outermost lines are not well sampled. This might indicate that the large molecular cloud surrounding this source (Loren 1989) contributes to the observed C$^{18}$O lines. We tested a core that has a warm envelope surrounding an inner, denser core. The core has the same density and temperature structures inside 0.15 pc as those calculated from dust emission, and a constant density and temperature of 10$^4$ cm$^{-3}$ and 50 K from 0.15 to 0.6 pc, which are based on the $^{13}$CO observations (Loren 1989). A temperature of 50 K is the upper limit in the $\rho$ Oph molecular complex. The modeled line profiles are shown in Figure 7c and fit the observed line profiles better than those in the previous model, which does not have a warm envelope. In this model, the abundance distribution is the same as the previous one. In order to avoid confusion by the envelope, we need to use a rarer

![Fig. 7a](image_url)

**Fig. 7a**

(a) Results of the MC modeling in the C$^{18}$O J = 2–1 line. The C$^{18}$O J = 2–1 and J = 3–2 lines have been modeled simultaneously, and we choose the abundance structure that fits both of the lines. In each panel, the solid and the dashed lines indicate the modeled and the observed line profiles, respectively. The arcseconds marked in the middle panels represent the angular distance from the dust peak of each core. (b) Results of the MC modeling in the C$^{18}$O J = 3–2 line. (c) Results of the MC modeling of L1689B in the C$^{18}$O lines including a warm envelope.
Fig. 7b

Fig. 7c
isotope or higher J transition to trace the high-density core. Even though L1512 and L1544 are believed to be well isolated, they might also be surrounded by bigger clouds. The modeled results, however, fit well the observed C18O J = 2–1 line to the off-position of 90″. The influence of bigger structures in L1512 and L1544 does not seem significant compared to L1689B.

Jessop & Ward-Thompson (2001) modeled the C18O J = 2–1 and J = 3–2 lines of L1689B using a density structure with the same central density (ρ_{flat}) and the same R_{flat} as calculated by André et al. (1996) and a constant temperature. After comparing to observations, they argued that the flat distribution of C18O is caused by the significant (about 95%) depletion of CO. They pointed out that the gas temperature must be above 14 K to have better agreement with observations. However, they compared the model to the observation within 32″, which cannot give a good constraint on the outer envelope. In addition, the lower density and higher temperature at the inner region than those assumed in this study make the transitions optically thinner than the actual lines, so the depletion factor to fit the observations could be overestimated. We model C18O lines using our density structure and a constant temperature of 14 K. The best-fit model has r_D ~ 0.035 and f_D ~ 10, which are greater than our best-fit model, where the temperature structure is calculated from the analysis of dust emission. The modeled C18O J = 2–1 lines within 60″ are stronger than the observed lines. However, the line at 90″ is still weaker than the observed line even though it is stronger than in our best-fit model without a warm envelope.

5.3.2. H^13CO^+ J = 1–0 and J = 3–2

Except for the C18O lines, X_0 is not fixed in modeling molecular lines, but it can be easily decided by the outermost line profile. The results of the best models in H^13CO^+ J = 1–0 and J = 3–2 are shown in Figure 8 and Table 8. We have observed the H^13CO^+ J = 1–0 line with a 20″ grid out to the distance of 60″ from the center with an 18″ beam. The J = 3–2 line has been observed with 30″ spacing with a 26″ beam. In L1512, the H^13CO^+ J = 3–2 line, whose critical density is about 10^6 cm^{-3}, was not detected, so we simulate only the J = 1–0 line. The depletion factor in L1512 is 25 within 0.021 pc (38″). In L1689B, the best-fit model of the J = 1–0 line also fits the J = 3–2 line very well. The depletion factor and radius in L1689B are much smaller than those in L1512. However, the undepleted abundance of H^13CO^+ in L1512 is 1.4 times greater than in L1689B.

The observed H^13CO^+ J = 1–0 line, whose critical density is about 10^5 cm^{-3}, shows a blue skewed profile in L1544. Contracting cores show stronger blue peaks and self-absorption dips in optically thick lines (Myers et al. 1996). Evidence of inward motion in L1544 has been observed by Tafalla et al. (1998) and Williams et al. (1999). Therefore, we used the best-fit Plummer-like model in the simulation of the H^13CO^+ J = 1–0 line. In L1544, models fit well the shapes of the observed H^13CO^+ J = 1–0 line profiles, but the modeled J = 3–2 line is stronger than the observed line by a factor of 2. The rms noise of this line is about 0.015 K (5 σ detection), and the baseline is poor, so the discrepancy may not be very significant. There are several possibilities. If there were molecular gas surrounding L1544, this less dense gas would increase the J = 1–0 line more than the J = 3–2 line. Therefore, our models would overestimate the abundance of the inner, denser core to fit the J = 1–0 line. As a result, the modeled J = 3–2 line could be stronger than the observed line. Another possible explanation is that the depletion fraction increases toward the denser, inner region. Since the J = 3–2 line traces denser gas than the J = 1–0 line, the J = 3–2 line in our models where we used a step function for the abundance would be stronger than the observed line if H^13CO^+ were depleted more at the center. The uncertainties in the observed line or in the density and temperature structures could explain the difference between the modeled and observed lines.

5.3.3. DCO^+ J = 3–2

The modeling of DCO^+ J = 3–2 does not constrain free parameters well because the observations in the line do not cover positions far from the center. The results are shown in Figure 9 and in Table 9. In L1512, only the center position was observed, so we simply used a constant abundance to fit the line profile. The abundance of DCO^+ that fits the line profile well is 2.8 × 10^{-10}. However, the line profiles of two positions in L1544 and three positions in L1689B were compared with the results of models. The factor and the radius of the depletion of the DCO^+ molecule are much smaller than those of the CO molecules calculated by simulating the C18O J = 2–1 and J = 3–2 lines. This result is consistent with the results of the chemical model of Caselli et al. (2002). The radius of the depletion is less (20″) than the first line.
5.3.4. HCO\(^+\) J = 3–2

Infall asymmetry in PPCs has been observed (Tafalla et al. 1998; Lee, Myers, & Tafalla 1999; Gregersen & Evans 2000) in optically thick lines. If the gas of the outermost envelope of a core that has inward motion has sufficient optical depth and has a lower excitation temperature than the gas of the inner envelope in a given molecular line, the molecular line shows infall asymmetry, in which the intensity ratio of the blue peak to the red peak increases with time (Gregersen et al. 1997). We model one of the optically thick lines, HCO\(^+\) J = 3–2, in the three PPCs and compare the results with the observational results of Gregersen & Evans (2000). In order to model an HCO\(^+\) J = 3–2 line that has infall asymmetry, we use the best-fit Plummer-like model. Figure 10 shows the difference in MC modeling of the HCO\(^+\) J = 3–2 line for two different physical models: the Bonnor-Ebert sphere and the Plummer-like model. The latter includes an infall velocity structure and produces a blue asymmetry. The HCO\(^+\) J = 3–2 line in L1512 does not show a self-absorption dip and asymmetric profile, so we model the line in L1512 using the best-fit Bonnor-Ebert sphere.

The results of modeling the HCO\(^+\) J = 3–2 line in the three PPCs are shown in Figure 11 and in Table 10. Because L1512 has only one spectrum at the position 30\(^\circ\) away from the center, we use a constant abundance of HCO\(^+\) for this core. The abundance of the best fit is about \(1 \times 10^{-9}\). In L1544, the intensity of the HCO\(^+\) J = 3–2 line at 30\(^\circ\) is half that at the center, unlike the \(^{13}\)CO\(^+\) (1–0) line, whose intensity is almost flat to 40\(^\circ\). As a result, an exponential abundance distribution as well as a step function also fits well the line profiles. In L1689B, the HCO\(^+\) J = 3–2 line has a stronger red-peak asymmetry at the center and 15\(^\circ\) away, but it has a stronger blue-peak asymmetry at 30\(^\circ\) and 45\(^\circ\). This complication of line profiles causes difficulty in fitting the exact line profiles in this core. Therefore, we tried to

![Figure 8a](image_url)

**Fig. 8a** — (a) Results of the MC modeling in the \(^{13}\)CO\(^+\) J = 1–0 line. The \(^{13}\)CO\(^+\) J = 1–0 and J = 3–2 lines have been modeled simultaneously, and we choose the abundance structure that fits both of the lines. In order to model these line profiles, in L1512 and L1689B we use the density and temperature profiles given by Bonnor-Ebert dust models (Evans et al. 2001), but we calculate the structures of density and temperature in L1544 combining the empirical dynamics model of Whitworth & Ward-Thompson (2001) and the dust radiative transfer code. (b) Results of the MC modeling in the \(^{13}\)CO\(^+\) J = 3–2 line.
Fig. 8b

Fig. 9.—Results of the MC modeling in the DCO$^+$ $J = 3–2$ line
fit the integrated temperatures of the lines with radius. The exponential function of the abundance shows results similar to the step function. In order to test the functional form of the abundance, we need a more extended map. The interesting result is that the HCO$^+$ $J = 3–2$ line of L1689B has a strength similar to that of L1544, unlike H$^{13}$CO$^+$ (1–0), which is stronger in L1689B than in L1544. This might be due to the fact that L1689B is embedded in a larger molecular cloud that causes more absorption of the HCO$^+$ (3–2) line.

On the whole, the abundance of HCO$^+$ in this result is very small compared to the abundance that is expected from H$^{13}$CO$^+$ and the typical ratio of C and $^{13}$C in the local interstellar medium of about 77 (Wilson & Rood 1994). However, our results show that the abundance ratio of HCO$^+$ and H$^{13}$CO$^+$ is approximately from 3 to 15 in the three PPCs. (We do not think that the ratio in L1512 is correct because we used only one spectrum in each line to calculate the abundance.) In addition, the depletion factors and the depletion radii calculated from the HCO$^+$ line are different from those calculated from the H$^{13}$CO$^+$ lines. These differences and the low abundance ratio may result from the gas components outside the cores that we model in this study because the HCO$^+$ line can trace less dense gas than H$^{13}$CO$^+$. As a result, the HCO$^+$ line can be absorbed by the surrounding material significantly, but the H$^{13}$CO$^+$ line may be not absorbed as much as the HCO$^+$ line. In our models, we limit the size of every core to 0.15 pc, so our models cannot account for the gas outside the core. Thus, we would have underestimated the abundance trying to fit a line that has been weakened by the absorption by the surrounding gas component. However, this explanation is just one possibility. We cannot ignore the uncertainties of many other parameters, so we leave this as future work.

6. DISCUSSION

6.1. Depletion

We conclude that CO is significantly depleted in L1512 and L1544. It is difficult to estimate the depletion of CO in L1689B because of the gas surrounding this core and the optical depths of the lines used, but the depletion appears to be much less. The HCO$^+$ molecule is depleted in L1512 and L1544, but we do not see significant depletion of this molecule in L1689B, based on modeling the H$^{13}$CO$^+$ $J = 1–0$ line. The optical depth and possible surrounding material also affect the calculation of the depletion of HCO$^+$ in L1544. DCO$^+$ is not significantly depleted in any of the PPCs. This result is consistent with results in many other starless cores where the distribution of DCO$^+$ fits well the distribution of dust continuum (P. C. Myers 2002, private communication). However, we need to use better resolution to do a more precise study because the calculated depletion radius is not greater than the actual beam size (35″). Caselli et al. (2002) show that the depletion radius of DCO$^+$ is about 3000 AU in L1544.

The analysis of the integrated intensity shows that the earliest time molecule CCS is not peaked toward the centers of any of the PPCs, unlike the dust emission. Thus, CCS is depleted significantly in all three. As we saw, however, the CCS intensity in L1544 is 2 times stronger than that in L1689B even though the dust emission of L1689B and L1544 is similar. This result suggests that the depletion of CCS is connected to the depletion of CO. Li et al. (2002) modeled chemical abundance changes in PPCs using a dynamical model with a magnetic field, which drives the ambipolar diffusion, and they got a relatively high abundance of CCS. They indicated that this abundance could result from the interplay between significant depletion of CO molecules and late-time hydrocarbon chemistry. Ruffle et al. (1997, 1998) also showed the same result in their models of the time dependence of several molecules. According to their models, the abundance of CCH and CCS have later secondary maxima only when the freeze-out timescale is

![Fig. 10.—Comparison of the MC modeling in the HCO$^+$ $J = 3–2$ line of L1544 for two different physical models: the Bonnor-Ebert sphere and the Plummer-like model (see Fig. 4). Both have the same abundance structure, but only the Plummer-like model, with an infall velocity structure, produces the blue asymmetry shown in observed line profiles.](image-url)
long compared to the chemical timescale or the collapse timescale. CCS increases quickly to the first maximum of its abundance in time and is depleted very early as the density increases because CCS is destroyed by increasing HCO\textsuperscript{+} or H\textsubscript{3}O\textsuperscript{+}, and this polar molecule can be tightly bound in grain mantles. However, in the region where CO molecules are depleted significantly, the C\textsuperscript{+} ion reacts more with molecules that are not oxygen-bearing species, so the precursors of CCS such as CCH increase again. This results in a second increase of the CCS abundance. The trend did not show up in the models of Bergin & Langer (1997) and Aikawa et al. (2001) because the models used dense initial conditions in which a core evolves very quickly dynamically and CCS did not show the second maxima. We think that the CCS molecule is possibly in the second enhancement in the late stage of chemical evolution resulting from the significant depletion of CO in L1512 and L1544. The integrated intensity of the CCS line shows bumps in the center regions of L1512 and L1544 (Fig. 3). If CCS were depleted with time without the second enhancement, we would see holes rather than bumps. The other possible explanation of the enhancement of CCS is the mixing of some atomic carbon from a translucent envelope into the core (E. F. van Dishoeck 2002, private communication).

According to the comparison between the intensity of N\textsubscript{2}H\textsuperscript{+} lines and the dust emission intensity, this molecule is possibly depleted in L1512 but not in L1544 and L1689B, where its intensity follows well the dust emission intensity. N\textsubscript{2}H\textsuperscript{+} is known as a very late time molecule, but Bergin et al. (2002) have shown that N\textsubscript{2}H\textsuperscript{+} is depleted in a cold dark cloud, B68. The weak intensity of the N\textsubscript{2}H\textsuperscript{+} line in L1689B, compared to in L1544, might indicate that this molecule has not yet reached its maximum because of less abundant precursors (N\textsubscript{2} and H\textsubscript{3}\textsuperscript{+}) but a more abundant destroyer (CO).

Bergin & Langer (1997) modeled chemical evolution in PPCs, including gas-grain interactions as well as gas-phase...
reactions, and compared two kinds of grain mantle properties: a weakly bound CO mantle and a tightly bound H$_2$O mantle. Their results show that sulfur-bearing molecules such as CS and SO are very sensitive to density and depleted seriously as the density of a core increases, regardless of the properties of dust grains. On the other hand, CO and HCO$^+$ molecules are depleted in the model with H$_2$O grain mantles but remain in the gas phase in the CO grain mantles. In contrast, NH$_3$ and N$_2$H$^+$ do not show depletion in any model because of the low binding energy of N$_2$ to H$_2$O and CO mantles. Therefore, the comparison of the results of their chemical models to our results indicates that the dust grains in the three PPCs have tightly bound H$_2$O mantles. In addition, Aikawa et al. (2001) predicted the results of their chemical models to our results indicates that the depletion factor of CO, which are not well known. We suppose that the depletion of atomic oxygen might be significantly depleted in L1512 and in L1544. According to their results, CCS and CO molecules are depleted, but N$_2$H$^+$ and NH$_3$ molecules are more abundant in more slowly collapsing cores at the density peak.

To summarize our results on depletion, CCS, CO, and HCO$^+$ are significantly depleted in L1512 and in L1544. On the other hand, the depletion of DCO$^+$ in the two cores is not significant. N$_2$H$^+$ is not depleted in L1544, but it is possibly depleted in L1512. In contrast, only CCS is significantly depleted in L1689B. It is difficult for us to estimate the depletion of CO in L1689B because of the optical depth effect and the material surrounding the cores.

### 6.2. Ionization

The coupling between ions and the magnetic field is crucial in regulating star formation rates if cores are magnetically subcritical. The timescale of ambipolar diffusion depends on the ionization fraction \( \tau_{AD} \approx 2.5 \times 10^{13} x(e) \) (Shu et al. 1987). In addition, the gas-phase chemical reactions are also dependent on the ionization fraction. Therefore, calculating the ionization fraction accurately is significant for understanding the chemistry as well as the timescale for ambipolar diffusion. However, it is not easy to calculate the ionization fraction in protostellar cores because it depends on the depletion of molecules as well as density structures and the cosmic-ray ionization rate.

We use equation (16) in Caselli (2002) to calculate the ionization fraction:

\[
x(e) = \frac{2.7 \times 10^{-8}}{[\text{DCO}^+]/[\text{HCO}^+]} - 1.9 \times 10^{-7} \left[ \frac{1}{f_D} + \frac{x(\text{O})/f'_D}{10^{-4}} \right],
\]

where \( f_D \) is the depletion factor of CO, \( x(\text{O}) \) is the abundance of atomic oxygen (1.5 \times 10^{-4}; Caselli et al. 1998), \( f'_D \) is the depletion factor of O, and \([\text{DCO}^+]/[\text{HCO}^+]\) is the abundance ratio of the two molecules, which can be calculated by comparing the column densities of DCO$^+$ and H$^{13}$CO$^+$ and using 77 \pm 7 for the $^{12}$C/$^{13}$C ratio (Wilson & Rood 1994). Caselli et al. (1998) and Caselli (2002) derived this equation assuming that (1) the main source of HCO$^+$ is the reaction between H$_3^+$ and CO, (2) the deuterium fractionation is due to the reaction between H$_3^+$ and HD, and (3) molecular ions are destroyed mainly by electrons and neutral species such as CO and O. In fact, Caselli et al. (2002) have shown that N$_2$H$^+$ and N$_2$D$^+$ are better tracers of the ionization fraction because HCO$^+$ and DCO$^+$ are possibly depleted in the central region. However, we do not have N$_2$D$^+$ data, so we use DCO$^+$ and HCO$^+$, which can give correct information in the region with \( r > 3000 \) AU.

We calculate, for each line of sight, the average \( x(e) \) along the line of sight. This approach is not completely self-consistent because the method is valid only for homogeneous clouds. We use our model to simulate observation with the same beam size. The column density of each molecule has been calculated from the simulated line based on the assumption of an optically thin line. Figure 12 shows the ionization fraction with radius in the three PPCs.

There are some caveats in this calculation. First, we cannot assess the depletion factor of CO in L1689B correctly because of the optical depth problem and the possible material surrounding the core (§ 5.3.1). Second, the model of the H$^{13}$CO$^+$ lines in L1544 does not match the observations very well, so that the calculated column density from the simulated H$^{13}$CO$^+$ is not significant. Third, since we do not have enough observed data to assess the depletion radius of DCO$^+$ in L1512, the column density of DCO$^+$ is uncertain in this core too. In addition to the caveats related to models, the equation that we used to calculate the ionization fraction includes the abundance and the depletion fraction of O, which are not well known. We use \( f_D = 3, 2, 1 \) for L1512, L1544, and L1689B, respectively.

In spite of these caveats, the three cores have similar average ionization fractions (\( \approx 5 \times 10^{-7} \)) along the line of sight toward the centers. These results are similar to the ionization fractions calculated in other protostellar cores (Caselli et al. 1998) but much greater than the result (\( \approx 10^{-9} \) at the

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**Fig. 12.**—Ionization fractions in the three PPCs. The error bars represent the amount of uncertainty in the ionization fraction when the ratio of DCO$^+$ to HCO$^+$ and the depletion fraction of the CO molecule change by up to 30% of the calculated values in each point.
center) of Caselli et al. (2002). Caselli et al. (1998) have used the integrated temperatures of the actual line profiles, but Caselli et al. (2002) have used the results of their “L1544 best-fit” chemical model, which takes into account the cloud density structure, molecular freeze-out, and the recombination of molecular ions on grain surfaces, in order to infer the electron fraction as a function of cloud radius. Our data do not rule out still smaller values of \( x(e) \) at small radii. The ionization fraction in L1512 and L1544 decreases toward the center, which trend has been shown in Caselli et al. (2002) and Caselli (2002). In contrast, in L1689B it increases toward the center. As a result, the ionization fraction of L1689B around 0.06 pc is smaller than those of L1512 and L1544 by a factor of 10.

### 6.3. Timescales

The timescale of ambipolar diffusion \( [\tau_{AD} \approx 2.5 \times 10^7 x(e); \text{Shu et al. 1987}] \) calculated from the above ionization fraction toward the centers is about \( 1.25 \times 10^7 \) yr. This timescale applies to cores that are magnetically subcritical. This ambipolar timescale represents the duration of contraction from the present stage to the stage of Class 0. This is much greater than the free-fall timescale \( (\approx 10^5 \) yr). However, \( x(e) \) could be much smaller at the center. Even though these three cores have similar ambipolar diffusion timescales toward the center, our results suggest that they have different chemical statuses.

L1512 seems to have evolved chemically more than L1544, showing that CCS, CO, HCO\(^+\), and possibly N\(_2\)H\(^+\) are depleted. Caselli (2002) modeled a core that is less dense and less centrally concentrated than L1544 to show the chemistry in an early stage in the dynamical evolution. According to their result, molecules in the model core are not significantly depleted. The model core is similar to L1512 in density structure, but surprisingly, L1512 shows a greater depletion radius of CO than L1544. In addition, N\(_2\)H\(^+\) at the center of L1512 might be starting to be depleted. This could result from the slower contraction of L1512 than L1544, so L1512 could have a longer time to evolve chemically. Another possibility is a more efficient molecular freeze-out in L1512 because the dust grains in this object are smaller than in the other two cores, so that the depletion timescale in L1512 is shorter (van Dishoeck et al. 1993; P. Caselli et al. 2003, in preparation). This could be possible because L1512 is less dense than the other two cores and has not had enough time for grain coagulation (Evans et al. 2001).

On the other hand, L1689B has not evolved much chemically, even though the density structure is very similar to L1544, so it is in a later stage of dynamical evolution than is L1512. This tells us that the chemical evolution is not a simple function of density, unlike the results of other chemical models. According to this result, we should not ignore the possibility that L1689B could be magnetically supercritical and that the core has evolved faster dynamically than the other two sources, so that L1689B has not had enough time to evolve chemically. The broader lines in L1689B (Fig. 1; § 3.1) indicate more active kinematics than the other two sources. The total masses of L1544 and L1689B are similar according to the dust modeling. Therefore, L1689B has to have a weaker magnetic field or a smaller ionization fraction in order to be magnetically supercritical. Crutcher & Troland (2000) measured the magnetic field along the line of sight in L1544 (\( B_{LOS} \approx 11 \text{ \mu G} \)) by using the Zeeman effect of the OH lines. There is no specific measurement of magnetic fields in L1689B. However, Troland et al. (1996) measured an OH Zeeman effect in the \( \rho \text{ Oph} \) cloud indicating \( B < 10 \text{ \mu G} \). In addition, our calculation shows that the ionization fraction in L1689B is smaller than in the other two cores in the outer part, where the calculation is more credible. The other possibility for the faster dynamical evolution of L1689B than L1544 is a larger external pressure (Galli, Walmsley, & Gonçalves 2002) because L1689B is in the \( \rho \text{ Oph} \) complex (see § 5.3.1).

Based on our results, we suggest that the stage of dynamical evolution of a core cannot be probed simply by its chemical status because the chemical evolution depends on the size of the dust grains and the absolute timescale during which the core has been in a given environment, as well as its density structure, which shows the relative stage of dynamical evolution. We summarize the dynamical and chemical evolutionary stages of each core in Table 11.

### 7. SUMMARY

The summary of our results is as follows:

1. The difference between the column densities inferred from dust emission and the emission of a given molecular line can partially result from the optical depth of the line. However, the depletion of a molecule must explain the remaining difference. In L1689B, the main cause of the difference between the dust emission and the CO emission is the optical depth in the lines. However, in L1512 the depletion of CO is the major source of the difference between the dust emission and the CO emission.

2. In our Monte Carlo simulation of molecular lines, a step function with depletion in the inner region produces the best fit to the abundance variation of a molecule in PPCs.

3. The CO and HCO\(^+\) molecules are depleted significantly in L1512 and L1544 but not in L1689B. The gas around L1689B makes it difficult to calculate the actual depletion of CO.

4. The depletion of DCO\(^+\) is not substantial in the three PPCs.

5. The CCS molecule is substantially depleted in the three PPCs. However, CCS might be in the second enhancement
in L1512 and L1544 because of the significant depletion of CO.

6. The distribution of the integrated intensity of N$_2$H$^+$ $J = 1-0$ suggests the possible depletion of N$_2$H$^+$ in L1512. On the other hand, N$_2$H$^+$ follows dust emission very well in L1544. In L1689B, N$_2$H$^+$ has not had enough time to reach its maximum.

7. The velocity structures calculated by a simple dynamical model that uses a Plummer-like density profile and a free-fall collapse model can produce the asymmetry of the HCO$^+$ $J = 3-2$ lines in L1544 and L1689B. However, the abundance calculated by modeling the lines is much smaller than what is expected from modeling H$^{13}$CO$^+$. The surrounding gas could possibly account for the low HCO$^+$ abundance of the models.

8. The ionization fraction is similar toward the centers of the three cores even though L1512 is less centrally condensed than L1544 and L1689B. However, L1512 has a bigger depletion radius of CO than L1544 and possible depletion of N$_2$H$^+$ at the center. In contrast, L1689B does not show the maturity in chemical evolution compared to the other two cores. This difference suggests that the chemical evolution depends on the size of dust grains and the absolute timescale during which a core stays in a given environment, as well as the density structure of the core, which shows the relative dynamical evolutionary stage.

9. The evolved density structure and the young chemistry of L1689B suggest that this core is possibly experiencing a free-fall collapse rather than ambipolar diffusion. As a result, L1689B evolves dynamically too fast to evolve chemically. This would be possible if the magnetic field in L1689B were weak enough or the external pressure were big enough to make L1689B magnetically supercritical.

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