Tuning pairwise potential can control the fragility of glass-forming liquids: from a tetrahedral network to isotropic soft sphere models

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Abstract. We perform molecular dynamics simulations for a SiO\(_2\) glass former model proposed by Coslovich and Pastore (CP) over a wide range of densities. The density variation can be mapped onto the change of the potential depth between Si and O interactions of the CP model. By reducing the potential depth (or increasing the density), the anisotropic tetrahedral network structure observed in the original CP model transforms into the isotropic structure with the purely repulsive soft-sphere potential. Correspondingly, the temperature dependence of the relaxation time exhibits the crossover from Arrhenius to super-Arrhenius behavior. Being able to control the fragility over a wide range by tuning the potential of a single model system helps us to bridge the gap between the network and isotropic glass formers and to obtain the insight into the underlying mechanism of the fragility. We study the relationship between the fragility and dynamical properties such as the magnitude of the Stokes–Einstein violation and the stretch exponent in the density correlation function. We also demonstrate that the peak of the specific heat systematically shifts as the density increases, hinting that the fragility is correlated with the hidden thermodynamic anomalies of the system.

Keywords: slow relaxation and glassy dynamics, structural glasses (theory)
1. Introduction

The current understanding of the mechanism behind the dramatic slowing down of supercooled liquids near glass transition temperatures still remains far from complete. Although the underlying mechanism of the glass transition is believed to be universal, many dynamical properties of the glass formers are diverse and system-dependent. Among them, the concept of the fragility, or the temperature dependence of the relaxation time and transport coefficients, such as the viscosity and diffusion constant, is one of the most important but least understood problems. For some glass formers, which are called strong liquids according to the Angell’s classification, the relaxation times obey the Arrhenius law, while others, called fragile liquids, show a strong departure from the Arrhenius law in their temperature dependence of the relaxation times \[1, 2\]. Representative strong glass formers are SiO\textsubscript{2} and GeO\textsubscript{2}, whose local molecular configurations are characterized by anisotropic network structures. On the other hand, fragile liquids such as \(\alpha\)-terphenyl and toluene tend to have more isotropic and compact local structures. The concept of fragility has played a key role in the study of glass transition. Many experimental studies have reported that there exist correlations between the fragility and various thermodynamic, structural, mechanical, and dynamical properties of the glass formers \[2\]. For example, it has been observed that the entropy and specific heat \[1, 3\], the elastic constants \[4, 5\], and the spatially heterogeneous dynamics \[6, 7\] sensitively depend on the fragility of the systems. Theoretical
understanding of the fragility, on the other hand, is left at the phenomenological level. Virtually all theoretical scenarios of the glass transition proposed so far, including the Adam–Gibbs theory [8], the random first order transition theory [9], energy landscape picture [10], geometric frustration scenarios [11–14], elastic models [15, 16], soft modes [17], and the dynamic facilitation scenario [18], have their own explanations of the fragility, but the first-principles and microscopic theory to quantitatively describe the fragility is still lacking [10, 19–22].

The difficulty of gaining a unified picture of the fragility from the experimental observations is obviously due to the diversity and complexity of real molecular or polymeric glass formers. The computer simulation is an ideal tool to avoid this difficulty because one can gain all microscopic information of dynamics for relatively simple model systems. Popular glass former models in the simulation studies, such as the soft-sphere (SS) [23] and the Lennard-Jones (LJ) potential liquids [12, 24, 25], are regarded as typical fragile glass formers. On the other hand, strong glass former models with anisotropic networks, where the particles are connected by covalent bonds, such as SiO₂ and GeO₂, have also been studied extensively by simulations [26–29].

There have been several attempts to understand the origin of the fragility systematically by simulations. In many studies, the isotropic potential systems, such as the SS and LJ potentials, have been employed. The fragility has been controlled using various methods, for example, by varying the density or pressure of the system [30–34], by changing the polydispersity [35–37] and the size ratio of the multi-component mixtures [12, 38], by tuning the interaction potential [31, 39, 40], or by truncating the attractive part of the LJ potential [41, 42]. The fragility was also found to be sensitive to many-body interactions which influence the local geometrical frustration [43, 44]. An idea to sort out thermodynamic and purely kinetic contributions to the fragility has been discussed recently [45]. The external parameters such as the impurities [46, 47] and the curvature of the non-Euclidean space [48] have been proposed as a new method to control the fragility. The findings of these studies, however, are still not sufficient to unravel the entire picture of the fragility. Aside from the obvious drawback that the time window which the current simulation can cover is narrow compared with the experiments, one of the obstacles of the computational studies is that the variation of the fragility which the simple glass former models can encompass is small [12, 30–32, 35–42]. Furthermore, the variation of the fragility is often masked by an apparent density-temperature scaling law, which makes it difficult to extract the generic mechanism controlling the fragility [31, 32]. There also remains the nagging question of how to decompose the kinetic and purely thermodynamic contributions of the fragility [45]. Even more important is to bridge the gap between the fragile isotropic systems and the strong network glass formers, which has been studied almost in different arenas in the past. Given these circumstances, it is beneficial to consider a simple model system which can cover a wide range of fragility, spanning from the strongest network glass former down to a very fragile isotropic system, simply by tuning a system parameter.

In this paper, we numerically study a simple model glass former originally introduced by Coslovich and Pastore (CP) as a model strong glass former mimicking SiO₂ [29]. The CP model is a binary mixture of spherical atoms interacting with the isotropic LJ potential with a very strong attraction between Si and O atoms, which allows them to form anisotropic tetrahedral network structures. In this study, the fragility of
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the CP model is examined over an extremely wide range of density from the order of unity up to virtually infinity. Varying the density is equivalent to changing the potential depth between Si and O atoms of the CP model. By reducing this potential depth (or increasing the density), the anisotropic tetrahedral network structure observed in the CP model is eventually transformed into an isotropic structure with a purely repulsive soft-sphere potential. Thus, it enables one to control the fragility from strong to fragile systematically.

Here, we summarize the results of this paper. By extensive simulations, dependence of the structure on the density is monitored using the radial distribution functions, the static structure factors, and the coordination numbers. By measuring the temperature dependence of the relaxation time obtained from the density–density time correlation function, we observe that the fragility systematically changes from strong to fragile with the change of the structures. We carefully examine the density-temperature scaling for the temperature dependence of the relaxation time $[49-55]$. It is confirmed that the relaxation time does not collapse onto a master curve. This implies that the observed fragility variation is not superficial but is due to a qualitative change of the underlying mechanism controlling the slow dynamics. We investigate the correlation between the fragility and several dynamical observables, i.e. the magnitude of the Stokes–Einstein (SE) violation and the exponent of the stretched exponential relaxation of the density correlation function. It has been argued that these observables are manifestations of spatially heterogeneous dynamics, or the dynamical heterogeneities, and they are intimately correlated with the fragility $[56]$. We confirm that more fragile systems show stronger SE violation, whereas a clear-cut correlation between the stretch exponent and the fragility is not observed. Finally, we also discuss the possibility that the fragility is related to the peak position of the specific heat observed in its temperature dependence.

This paper is organized as follows. In section 2, we describe the details of the simulation methods. The numerical results are presented in section 3. Finally, we discuss our results and conclude in section 4.

2. Simulation methods

In this section, we describe the simulation methods.

2.1. The Coslovich–Pastore model

Coslovich and Pastore have introduced a simple SiO$_2$ (strong glass former) model $[29]$. Its dynamical and structural properties have been intensively investigated for fixed densities $[57-60]$. The advantage of this model is its simplicity compared to other established SiO$_2$ models $[26-28]$. Although its potential is given by a combination of the SS and LJ potentials, the atoms in the CP model form an anisotropic tetrahedral network structure similar to those of the realistic SiO$_2$ models $[29]$. According to $[61, 62]$, there are three conditions for a binary mixture with spherical potential to generate the tetrahedral network structure: (1) The composition ratio is $N_1 : N_2 = 1 : 2$, where
$N_1$ and $N_2$ are the number of particles for species 1 and 2, respectively. (2) The potential is non-additive, i.e. the range of the interaction between species 1 and 2 is not a simple sum of their diameters. (3) The attractive interaction between different species is strong. The CP model satisfies these conditions.

The CP model is a binary mixture in three dimensions whose composition ratio is $N_1 : N_2 = 1 : 2$ and the mass ratio is $m_2/m_1 = 0.57$. Species 1 and 2 correspond to Si and O atoms of SiO$_2$, respectively. The interaction potentials between two particles are given by

$$v_{\alpha,\beta}(r) = \epsilon_{\alpha,\beta}\left\{ \left( \frac{\sigma_{\alpha,\beta}}{r} \right)^{12} - C(1 - \delta_{\alpha,\beta}) \left( \frac{\sigma_{\alpha,\beta}}{r} \right)^{6} \right\},$$

(1)

where $C$ is a constant which was set to unity in the original CP model [29]. We specify the particles by the Roman indices $i, j \in \{1, 2, \cdots, N\}$ and the species by the Greek indices $\alpha, \beta \in \{1, 2\}$. The parameters are set to $\epsilon_{12}/\epsilon_{11} = 24$, $\epsilon_{22}/\epsilon_{11} = 1$, $\sigma_{22}/\sigma_{11} = 0.85$, and $\sigma_{12}/\sigma_{11} = 0.49$. The last condition warrants that the potential is non-additive, i.e. $\sigma_{12} = (\sigma_{11} + \sigma_{22})/2$. $v_{\alpha,\beta}(r)$ is truncated at $r = 2.5\sigma_{\alpha,\beta}$. In order to ensure the continuity of the potential, we add a switching function, $S(r)$, up to $r = 3\sigma_{\alpha,\beta}$. The switching function connects two points, $R_1$ and $R_2$, continuously and is defined as

$$S(r) = \begin{cases} 
1 & (0 \leq r < R_1), \\
(r - R_2)^2(2r + R_2 - 3R_1)/(R_2 - R_1)^3 & (R_1 \leq r < R_2), \\
0 & (R_2 \leq r).
\end{cases}$$

(2)

We used $R_1 = 2.5\sigma_{\alpha,\beta}$ and $R_2 = 3\sigma_{\alpha,\beta}$.

2.2. Tuning of the potential depth

In this study, we introduce a parameter $C$ in the second term (the attraction part) of $v_{12}(r)$ in equation (1). $C$ is the strength of the attraction between different species. The depth of the potential well $\Delta$ is written in the unit of $\epsilon_{11}$ as $\Delta = \epsilon_{12}C^2/4\epsilon_{11}$. Hereafter, we use $\Delta$ instead of $C$. In figure 1, we show $v_{12}(r)$ for various $\Delta$’s, $\Delta = 6$ ($C = 1$) corresponds to the original CP model and $\Delta = 0$ ($C = 0$) corresponds to a simple SS potential. Note that the potential for $\Delta = 0$ is slightly different from the conventional SS potential model which has been extensively studied in the past [23], since the range of the interaction is still non-additive. Our model can seamlessly connect the original CP model with the purely repulsive SS potential model. As mentioned above, the atoms with large $\Delta$, i.e. strong attractive interaction, tend to form the tetrahedral network structure. This structure is broken as $\Delta$ reduces and eventually the local structure becomes isotropic and compact in the limit of $\Delta = 0$. Mathematically, changing $\Delta$ at a constant density $\rho$ is equivalent to changing $\rho$ at a constant $\Delta$. We explain the relation between $\Delta$ and $\rho$ using a simple scaling argument, following a similar argument for the SS potential model [63]. The Hamiltonian of the system is written as

$$\frac{H}{k_B T} = \frac{1}{k_B T} \left\{ \sum_{i=1}^{N} \frac{p_i^2}{2m_i} + \sum_{i<j} v_{\alpha,\beta}(r_{ij}) \right\},$$

(3)

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where $k_B$, $p_i$, $m_{\alpha i}$, and $v_{\alpha \alpha i}(r_{ij})$ are the Boltzmann constant, momentum, mass, and the potential given by equation (1), respectively. Introducing the unit of the length $\rho = \frac{1}{\tau l}$, this Hamiltonian can be rewritten as

$$
\frac{H}{k_B} = \Gamma^4 \left[ \sum_{i=1}^{N} \frac{p_i^2}{2m_{\alpha i}} + \sum_{i<j} \left\{ \left( \frac{\sigma_{\alpha \alpha i}^*}{r_{ij}^*} \right)^{12} - C(\rho \sigma_{11}^3)^{-2} (1 - \delta_{\alpha \alpha j}) \left( \frac{\sigma_{\alpha \alpha i}^*}{r_{ij}^*} \right)^6 \right\} \right],
$$

where $m_{\alpha i}^*$, $p_{\alpha i}^*$, $\sigma_{\alpha \alpha i}^*$, and $\epsilon_{\alpha \alpha i}^*$ are reduced parameters scaled by $m_i$, $m_i l / \tau_0$, $\sigma_{11}$, and $\epsilon_{11}$, respectively. The time unit is defined by $\tau_0 = \{ m_i l^2 / \epsilon_{11} (l / \sigma_{11})^2 \}^{1/2}$. $\Gamma \equiv \rho (\epsilon_{11} / k_B T)^{1/4} \sigma_{11}^3$ is a dimensionless parameter commonly used for the SS potential [63]. Note that there exist two dimensionless parameters which control the system: $\Gamma$ and $C(\rho \sigma_{11}^3)^{-2}$. This means that, for a fixed $\Gamma$ (or the temperature), changing the density with a fixed $C$ is equivalent to changing $C$ for a fixed density. Therefore, if one chooses the purely LJ system ($C = 1$) with a density $\rho_0$ as a reference system, one can infer thermodynamic and dynamical properties at arbitrary densities by tuning $C$ for the fixed $\rho_0$. The mapping from $C$ to $\rho$ is given by $(\rho_0 / \rho)^2 = C$, or equivalently in terms of $\Delta$ by

$$
\left( \frac{\rho_0}{\rho} \right)^2 = \frac{\Delta}{6}.
$$

From this mapping, one can cover the whole range of density up to $\rho = \infty$ by tuning $C$ (or $\Delta$) from a finite value down to 0.

### 2.3. Details of molecular dynamics simulations

We perform the molecular dynamics (MD) simulations for various $\Delta$’s. We use $\Delta = 6$, 2.667, 1.5, 1.042, 0.667, 0.375, 0.167, 0.042 and 0 at a constant density $\rho_0 = 1.655$. The correspondence of various $\Delta$’s for a fixed density $\rho_0$ to various densities for a fixed $\Delta = 6$ is summarized in table 1. By tuning $\Delta$, we explore a wide range of densities from 1.655 up to infinity of the original CP model. The number of the particles is
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3. Results

3.1. Structural properties

We first study the structural properties of the CP model for various potential depth \( \Delta \). We start with the radial distribution function \( g_{\alpha \beta}(r) \). Figure 2 shows \( g_{\alpha \beta}(r) \) for each \( \Delta \) at the lowest temperatures in our simulation which are listed in Table 1. For \( \Delta = 6 \) (see figure 2(d)), \( g_{12}(r) \) exhibits a very sharp peak at \( r \approx 0.6\sigma_{11} \), followed by the very broad and small first minimum which persists up to \( r \approx 3\sigma_{11} \) beyond which the small and broad second peak appears. In contrast, the first peaks of \( g_{11}(r) \) and \( g_{22}(r) \) are observed at \( r \approx 0.1 \) and \( r \approx 0.10 \), respectively. This indicates that the particles of species 1 and 2 are strongly bonded [29]. As \( \Delta \) decreases, the first peak of \( g_{12}(r) \) gradually decreases and broadens. Concomitantly the height of the first minimum rises to a finite value at around \( r \approx 0.1 \). Finally, at \( \Delta = 0 \) (see figure 2(a)), the profiles of \( g_{11}(r) \), \( g_{12}(r) \), and \( g_{22}(r) \) become similar to those of typical fragile glass formers such as the SS and LJ binary mixtures [23, 25]. This structural change reflects the fact that the bonds between species 1 and 2 are weakened by decreasing \( \Delta \).

To understand the effect of \( \Delta \) on the structure in more detail, we calculate the coordination number \( z_{\alpha \beta} \). \( z_{\alpha \beta} \) is the averaged number of the \( \beta \) particles in the first neighbor shell of the \( \alpha \) particle and defined by

\[
z_{\alpha \beta} = \rho_{\beta} \int_{0}^{r_{\alpha \beta}} dr 4\pi r^2 g_{\alpha \beta}(r),
\]  

Table 1. Summary of the parameters, \( \Delta \), the corresponding densities \( \rho \), and the temperature range of the present study.

| \( \Delta \) | \( \sqrt{\Delta} \) | \( \rho \) | \( T \) | \( k^* \) | \( T_{\text{onset}} \) | \( T_0^{(\tau_0)} \) | \( T_0^{(D)} \) | \( T^* \) | \( K^{(\tau_0)} \) | \( K^{(D)} \) |
|-------------|--------------|-------|--|--|----------------|----------------|----------------|-------|----------------|----------------|
| 0 | 0 | \( \infty \) | 0.07–0.34 | 5.8 | 0.18 | 0.0548 | 0.0547 | 0.085 | 0.372 | 0.475 |
| 0.042 | 0.204 | 5.733 | 0.06–0.34 | 5.9 | 0.16 | 0.0467 | 0.0465 | 0.065 | 0.357 | 0.459 |
| 0.167 | 0.408 | 4.054 | 0.57–0.34 | 5.9 | 0.12 | 0.0472 | 0.0461 | 0.11 | 0.162 | 0.759 |
| 1.042 | 1.021 | 2.564 | 0.065–0.34 | 5.6 | 0.14 | 0.046 | 0.0456 | 0.075 | 0.241 | 0.286 |
| 1.5 | 1.225 | 2.341 | 0.085–0.34 | 5.5 | 0.18 | 0.0599 | 0.059 | 0.11 | 0.2 | 0.229 |
| 2.667 | 1.633 | 2.027 | 0.14–0.6 | 5.2 | 0.26 | 0.0776 | 0.0793 | 0.2 | 0.1 | 0.126 |
| 6 | 2.449 | 1.655 | 0.3–1.25 | 5.0 | 0.48 | 0.161 | 0.173 | 0.4 | 0.087 | 0.123 |

Note: The peak position \( k^* \) of \( S_{11}(k) \), the onset temperature \( T_{\text{onset}} \) of the two-step relaxation, \( T_0 \) obtained by fitting the Vogel–Fulcher–Tammann (VFT) equations from the relaxation time \( \tau_0 \) and diffusion constant \( D \), the peak position \( T^* \) of the specific heat, and the fragility index \( K \) from \( \tau_0 \) and \( D \) are also tabulated.

\( N = N_1 + N_2 = 3000 \) with \( N_1 : N_2 = 1 : 2 \). The temperature range in which we perform the simulation are listed in Table 1. Hereafter, we use \( \sigma_{11}, \epsilon_{11}/k_B, \) and \( \sqrt{m\sigma_{11}^2/\epsilon_{11}} \) as the units of length, time, and temperature, respectively. The micro-canonical MD method with the periodic boundary condition is used to produce the trajectories. A time step \( \Delta t = 0.0005 \) is chosen throughout this study. For the calculations of the dynamic and thermodynamic quantities, we average over four independent simulation runs.
where \( \rho_\beta \) is the number density of species \( \beta \) and \( r^*_{\alpha\beta} \) is the position of the first minimum of \( g_{\alpha\beta}(r) \). In particular, \( z_{11} \) and \( z_{12} \) are useful to characterize the tetrahedral network structure. In SiO\(_2\), a single Si atom (species 1) is surrounded by four oxygen atoms (species 2), thus, \( z_{11} = 4 \), \( z_{12} = 4 \), and \( z_{21} = 2 \). In figure 2(f), we show \( z_{11} \) and \( z_{12} \) at the lowest temperatures for several \( \Delta \)'s. We use \( \sqrt{\Delta} \) instead of \( \Delta \) as the horizontal axis for the sake of visual clarity. At \( \Delta = 6 \) (\( \sqrt{\Delta} \approx 2.449 \)), we obtain \( z_{11} = 4 \) and \( z_{12} = 4 \), corresponding to the perfect tetrahedral network structure [29]. As \( \Delta \) decreases, both \( z_{11} \) and \( z_{12} \) increase. Eventually, we observe \( z_{11} \approx 14 \) and \( z_{12} \approx 9 \) at \( \Delta = 0 \). This indicates

\[ \text{Figure 2. (a)–(d) The radial distribution functions, } g_{11}(r), g_{12}(r), \text{ and } g_{22}(r), \text{ for several } \Delta \text{'s. The data for the lowest temperature for each } \Delta \text{ are shown. (e) } g_{11}(r) \text{ for several } \Delta \text{'s around 1. The vertical arrows are the position } r^*_{11} \text{ of the first minimum in } g_{11}(r). \text{ (f) The coordination numbers } z_{11} \text{ and } z_{12} \text{ as a function of } \sqrt{\Delta}. \text{ Data for the lowest temperatures are shown for each } \Delta. \text{ The open symbols are the results for the crystalline structure.} \]
that the tetrahedral network structure is broken and that the local configuration of the system becomes more isotropic and compact. We find that, in a narrow range of $\Delta$, $0.375 \leq \Delta \leq 0.667$ (or $0.612 \lesssim \Delta \lesssim 0.816$), the system crystallizes at low temperatures. Some of the samples in our simulation runs also crystallized at the lowest $T$ at $\Delta = 0.167$ and 1.042, when we carried out the simulation for a very long time ($t \gtrsim 10^6$). We show the results for the crystalline state by open symbols in figure 2(f). We confirm by carefully inspecting the real space snapshots that the systems crystallize completely over the entire simulation box. The coordination numbers for the crystallized samples are $z_{12} = 6$ and $z_{11} = 10$. This suggests that the observed crystalline structure is of Stishovite type. Indeed, it has been reported that SiO$_2$ forms the Stishovite crystal under very high pressures [64]. We remark that an exceptionally large value of $z_{11} \gtrsim 14$ at $\Delta = 1.042$ ($\Delta \approx 1.021$) is due to the ambiguity of defining the first coordination shell. As shown in figure 2(e), the profile of $g_{11}(r)$ is broadened around $\Delta \approx 1$, which makes it difficult to define $r_{11}^*$ clearly. Thus, $\Delta \approx 1$ can be regarded as the crossover regime from the network dominated region to the isotropic/compact structure region.

Next, we calculate the static structure factor $S_{\alpha\beta}(k)$. We show $S_{\alpha\beta}(k)$ at the lowest temperatures in figure 3 for several $\Delta$'s. At $\Delta = 6$, the maximal peaks are observed around $k \approx 8$ in all components of $S_{\alpha\beta}(k)$. These peaks originate from the tetrahedral structure whose bond length is estimated to be $2\pi/k \approx 0.79$. We also find weaker peaks at smaller wave numbers around $k \approx 5$. This is the so-called first sharp diffraction peak (FSDP) [65], which is known as an indication of the medium-range order of the length scale larger than the neighbor shell. In particular, the FSDP has been attributed to the formation of the hierarchical clusters of the tetrahedra with larger lengths [66]. When the potential depth $\Delta$ is reduced, these two peaks merge to a single peak. This result implies that the hierarchical tetrahedral structures disappear gradually as $\Delta$ is decreased. At $\Delta \lesssim 1$, the shape of the static structure factors are analogous to those observed in typical fragile glass formers such as the SS and LJ binary mixtures [67, 68].

3.2. Dynamical properties

As demonstrated above, the tetrahedral network structures are broken when the potential depth $\Delta$ is reduced to zero. In this section, we analyze the dynamical properties of the CP model. Specifically, the $\Delta$ dependence of the fragility is quantified.

First, we calculate the self part of the intermediate scattering function $F_k(t)$ for species 1 defined by

$$F_k(t) = \frac{1}{N_1} \sum_{i=1}^{N_1} \langle e^{-i k \cdot (r_i(t) - r_i(0))} \rangle,$$

where $r_i(t)$ denotes the position of the $i$th particle at time $t$. In figure 4, we show the temperature dependence of $F_k(t)$ for several $\Delta$'s. The wave number $k = |k|$ is chosen at the peak position $k^*$ of the static structure factor, $S_{11}(k)$ (see figure 3). The values of $k^*$ are listed in table 1. At high temperatures, $F_k(t)$ shows the exponential decay with the short relaxation time but, at low temperatures, dynamics dramatically slows down and $F_k(t)$ exhibits a two-step relaxation. This is the sign of the onset of the glassy dynamics.

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Figure 3. (a)–(d) The static structure factors, $S_{11}(k)$, $S_{12}(k)$, and $S_{22}(k)$, for several $\Delta$’s. The results for the lowest temperatures of our simulations are shown.

Figure 4. (a)–(d) The temperature variation of the self part of the intermediate scattering function for species 1 for several $\Delta$’s.
We define the relaxation time $\tau_\alpha$ by $F_s(k, \tau_\alpha) = e^{-1}$. We fit the observed $\tau_\alpha$ by the VFT equation:

$$\tau_\alpha \sim \exp \left[ \frac{1}{K(T/T_0 - 1)} \right],$$

where $T_0$ and $K$ are the fitting parameters. The parameter $K$ is referred to as the fragility index which is regularly used to quantify the degree of the super-Arrhenius temperature dependence [30]. The larger (smaller) values of $K$ correspond to the fragile (strong) glass formers. In this study, the VFT fitting is applied below $T_{\text{onset}}$, where the two-step relaxation for $E_s(k, t)$ sets in. $T_{\text{onset}}$ for each $\Delta$ is presented in table 1. We show the temperature dependence of $\tau_\alpha$ for several $\Delta$’s in figure 6(a). The temperature $T$ is scaled by $T_0$. It is clearly seen that the results for $\Delta = 2.667$ and $\Delta = 6$ follow the Arrhenius law at low temperatures [29]. For smaller $\Delta$’s, the temperature dependence of $\tau_\alpha$ deviates from the Arrhenius behavior. In other words, the system changes from strong to fragile glass formers with decreasing $\Delta$.

We also quantify the self diffusion constant $D_\alpha$ ($\alpha \in \{1, 2\}$) from the long-time behavior of the mean squared displacement (MSD). The MSD for species 1 is presented in figure 5. Figure 6(b) shows $(D_1/T)\sim^{-1}$ as a function of $T_0/T$.

The $\Delta$ dependence of the fragility index $K$ is demonstrated in figure 7. At $\Delta = 6$, the value of $K$ is small ($K \approx 0.1$), which is consistent with the results of the previous study [29]. As shown in figure 7, $K$ increases with a decrease in $\Delta$. At $\Delta = 1.042$ ($\sqrt{\Delta} = 1.021$), $K$ exceeds the value of the KA mixture, which is a typical fragile glass former ($K \approx 0.2$) [40]. We address the fact that the observed fragility index covers a wide range from $K = 0.087$ to $0.652$. In particular, the maximal value of $K = 0.652$ at $\Delta = 0.167$ is comparable with those of the most fragile glass formers studied in the simulations [14, 69]. $K$ is also obtained by using the VFT equation for $(D_1/T)\sim^{-1}$. The results are plotted with filled circles in figure 7. Although $K$ obtained from $(D_1/T)\sim^{-1}$ are larger than those obtained from $\tau_\alpha$ for all $\Delta$’s, the overall behavior is qualitatively the same. We remark that the increase of the fragility index with an increase in density has been reported for the BKS model [28], although the investigated densities were limited [70].

The observation that the system becomes the most fragile ($K$ becomes the largest) just next to the crystalline state may be related to the frustration scenario which claims that the fragility is controlled by the frustration against crystallization [71]. In fact, it has been reported that the system with a weaker frustration against crystallization tends to have larger fragility indices [36, 43]. Further investigation of the dynamics around this Stishovite-like crystallization regime would be valuable to verify the scenario.

In order to characterize the difference of dynamics between the strong (large $\Delta$) and fragile (small $\Delta$) regimes, we evaluate the ratio of the diffusion constants $D_2/D_1$ between species 1 and 2. In the experiments for $\text{SiO}_2$, it has been reported that the diffusion of Si and O atoms decouples at low temperatures and the ratio of the diffusion constants for Si and O, $D_{\text{O}}/D_{\text{Si}}$, increases with a decrease in temperature [72]. Similar behavior has also been demonstrated in simulations [73, 74]. As mentioned in [74], this decoupling is attributed to the rotational motion of the oxygen atom in the tetrahedral structure. In figure 8, we show $D_2/D_1$ as a function of $\tau_\alpha$ for several $\Delta$’s. At $\Delta = 6,$
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Figure 5. (a)–(d) The temperature variation of the mean squared displacement for species 1 for several $\Delta$'s.

Figure 6. The Arrhenius plots of the relaxation time (a) and of the diffusion constant for species 1 (b) as a function of the inverse temperature $1/T$. In both plots, the temperature is scaled by $T_0$, a fitting parameter of the VFT equation. The open symbols are the position of $T^*$ at which the specific heat shows the peak (see figure 12). The dashed straight lines indicate the Arrhenius temperature dependence.

$D_2/D_1$ increases with increasing $\tau_\alpha$ (with a decrease in temperature). This is consistent with the results for the original CP model [29]. As $\Delta$ decreases, the variation of $D_2/D_1$ becomes milder and eventually becomes almost a flat line at $\Delta = 0.167$. As $\Delta$ decreases further below $\Delta = 0.167$, the trend is reversed and $D_2/D_1$ becomes an increasing function of $\tau_\alpha$ again and the slope keeps increasing until $\Delta$ reaches 0, where the slope becomes maximum. The degree of the decoupling at $\Delta = 0$, which corresponds to the
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Figure 7. The fragility index $K$ as a function of $\Delta$. The results of the VFT fitting by $\tau_\alpha$ and $(D_2/T)^{-1}$ are shown as the squares and circles, respectively. The results of the Kob–Andersen (KA) mixture from Sengupta et al [40] are shown by the horizontal arrows. The gray shaded area indicates the region where we observe crystallization at lower temperatures.

Figure 8. The ratio of the diffusion constants $D_2/D_1$ as a function of $\tau_\alpha$ for several $\Delta$'s.

SS model, is even larger than that of the network glass former at $\Delta = 6$. Similar strong decoupling between $D_1$ and $D_2$ has been reported for the conventional SS model [75]. This non-monotonic $\Delta$ dependence of $D_2/D_1$ is another signature that the dynamics of the CP model are changed qualitatively by tuning the potential depth $\Delta$. It is natural to expect that the underlying mechanisms behind the strong decoupling of $D_1$ and $D_2$ at the two extreme ends of $\Delta = 0$ and 6 are completely different. It would be worthwhile seeking the origin of this strong decoupling for $\Delta = 0$.

3.3. Absence of the density-temperature scaling

The density-temperature (DT) scaling is a useful way to single out the parameter which controls the thermodynamic and dynamical properties of liquids. The simplest example
is the inverse power law (IPL) potential, \( v(r) \sim r^{-n} \), where the DT scaling exactly holds and the system is characterized by a single parameter, \( \rho^{\gamma}T \), where \( d \) is the spatial dimension [63]. It has been known that a broad class of liquids can be scaled by a single parameter \( \rho^{\gamma}T \), where \( \gamma \) is a constant [50, 52–55]. It has been argued that the DT scaling holds if there is a strong correlation between the virial \( W \) and the potential energy \( U \). The liquids for which the correlation between \( W \) and \( U \) is more than 90%, are called strongly correlating or Roskilde-simple liquids [52–55]. Since the CP model with \( \Delta = 0 \) is a purely IPL system, the DT scaling exactly holds. On the other hand, the previous study has demonstrated that at \( \Delta = 6 \) (non-IPL system), the correlation coefficient between \( W \) and \( U \) is less than 10% (non-strongly correlating liquid), thus the DT scaling does not hold [76]. Consequently, the validity of the DT scaling for the CP model varies depending on \( \Delta \).

There is another type of DT scaling where it is convenient to characterize the dynamical quantities such as the relaxation time \( \tau_\alpha(T) \). It has been argued that \( \tau_\alpha(T) \) for many liquids is scaled by the characteristic time and energy at high temperatures, \( \tau_\infty \) and \( E_\infty \). \( \tau_\alpha(T) \) and \( E_\infty \) are determined by fitting \( \tau_\alpha(T) \) at high temperatures using the Arrhenius law:

\[
\tau_\alpha(T) \approx \tau_\infty \exp[E_\infty(T\alpha)].
\]

This scaling has also been demonstrated to work well in many supercooled liquids and polymer systems [49–51].

As mentioned in section 1, the density or pressure dependence of the fragility has been studied in various systems [30–33]. However, some of those results can be collapsed onto a master curve using the DT scaling, which means that the observed variation of the fragility is only superficial with no physical significance [31, 32].

Here, we examine the DT scaling using equation (9), for the relaxation time \( \tau_\alpha(\Delta, T) \) of the CP model. In figure 9, \( \tau_\alpha(\Delta, T) \) scaled by \( \tau_\infty(\Delta) \) is plotted as a function of \( E_\infty(\Delta)/T \). In this figure, the potential depth \( \Delta \) is used instead of the density \( \rho \). At the small \( \Delta \) regime, the relaxation times are collapsed onto a master curve, whereas they systematically deviate from the master curve as \( \Delta \) increases. This result eloquently demonstrates that the dynamical properties of the CP model do not follow the DT scaling. From these results, it is concluded that the observed variation of the fragility is not superficial but it is a genuine manifestation of the changeover of the physical mechanism.

### 3.4. Stokes–Einstein violation and stretch exponent

The advantage of the CP model is that the correlation of physical quantities with the fragility can be studied systematically in a single system over a wide range of fragility. In particular, it enables one to examine the much debated issues on the relation of fragility with dynamical properties, such as the SE violation and the stretched exponential relaxation. In normal liquids, it is expected that the SE relation, \( D\eta/T \propto \text{const.} \) holds, where \( D \) and \( \eta \) are the diffusion constant and viscosity, respectively. However, the SE relation is violated in most supercooled liquids near the glass transition temperature. This SE violation is often regarded as a manifestation of the spatially heterogeneous dynamics, or the dynamical heterogeneities [56]. Previously, the SE violation of the
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original CP model \((\Delta = 6)\) has been investigated \([59, 60]\). These studies highlight the qualitative difference between the CP model \((\Delta = 6)\) and other fragile glass formers in their dynamical behavior \([77]\). The aim of this section is to elucidate the dependence of the SE violation on fragility in a systematic way.

In figure 10(a), we show the SE ratio, \(D_i(T)\tau_\alpha(T)/D_i(\text{onset})\tau_\alpha(\text{onset})\), normalized by the values at \(T_{\text{onset}}\), as a function of \(\tau_\alpha\). For all \(\Delta\)'s, the SE relation is violated, i.e. the SE ratio increases with an increase in \(\tau_\alpha\) (or a decrease in temperature). We remark that the deviation of the SE ratio at high temperatures (small \(\tau_\alpha\)) is an artifact caused by the use of \(\tau_\alpha\) instead of \(\eta/T\) \([59, 78, 79]\). Dependence of the SE violation on fragility is shown in figure 10(b). Here we plot the SE ratio at low temperatures (at \(\tau_\alpha = 10^4\)) against the fragility index \(K\). A clear correlation between the SE violation and the fragility is observed, that is, the more fragile systems tend to exhibit stronger SE violation.

Next, we study the stretch exponent \(\beta_{\text{KWW}}\) of the nonexponential relaxation observed in the density correlation function. Experimental studies have shown that the fragile systems tend to have smaller stretch exponents than the strong systems \([6, 7]\). Some theories explain this observation \([80]\), while others argue that there is no direct correlation between the fragility and \(\beta_{\text{KWW}}\) \([81, 82]\).

Figure 9. The density-temperature scaling for the relaxation time \(\tau_{\alpha}(\Delta, T)\) scaled by \(\tau_{\infty}(\Delta)\) as a function of \(E_{\infty}(\Delta)/T\). The straight line represents equation (9).

Figure 10. (a) The SE ratio as a function of \(\tau_\alpha\). The vertical dashed line corresponds to \(\tau_\alpha = 10^4\). (b) The SE ratio at \(\tau_\alpha = 10^4\) as a function of \(K\).
Here, we show the fragility dependence of the stretch exponents of the CP model. We determine $\beta_{\text{KWW}}$ from $F_k(t)$ using the following fitting function,

$$F_k(t) = (1 - f_c)\exp\left[-(t/\tau_s)^2\right] + f_c\exp\left[-(t/\tau_l)^{\beta_{\text{KWW}}}\right],$$

where $f_c$, $\tau_s$, and $\tau_l$ are fitting parameters [78]. Figure 11(a) shows $\beta_{\text{KWW}}$ as a function of $\tau_s$. For all $\Delta$’s, $\beta_{\text{KWW}}$ decreases gradually with an increase in $\tau_s$ (a decrease in temperature). In figure 11(b), we plot $\beta_{\text{KWW}}$ at $\tau_s = 10^4$ as a function of $K$. Surprisingly, we observe no clear correlation between the fragility and $\beta_{\text{KWW}}$, although $\beta_{\text{KWW}}$ becomes somewhat larger at a strong-liquid regime of $\Delta = 2.667$ and 6. This observation is not inconsistent with the argument in [82]. A similar trend has been reported for the harmonic sphere model [33].

### 3.5. Relationship with specific heat peak

Finally, we discuss the possible relationship between the thermodynamic properties and the fragility variation observed in the CP model. Several simulation studies using the BKS model [28] for SiO$_2$ have demonstrated that there exists the so-called fragile-to-strong (FS) crossover; the temperature dependence of the relaxation time changes from super-Arrhenius (fragile) to Arrhenius (strong) behavior with a decrease in temperature [73, 83, 84]. It has been argued that this FS crossover is related to a thermodynamic anomaly signaled by the appearance of the peak of the specific heat [83–85] which tends to shift to lower temperatures if the density is increased [83, 84, 86]. This anomaly might be connected to a hidden thermodynamic singularity such as the liquid–liquid transition, but the overall picture is still unclear. Under these circumstances, it is of great interest to examine whether the FS crossover and the shift of the specific heat are also observed in the CP model by tuning the potential depth $\Delta$.

The specific heat is calculated by $c_V = \frac{\partial U}{\partial T}$. Figure 12 shows the temperature dependence of $c_V$ for various potential depths $\Delta$. The temperature $T$ is normalized by the onset temperature $T_{\text{onset}}$. As observed, there exists the broad but clear peak of $c_V$ at a finite temperature $T^*$ for all $\Delta$’s except for $\Delta = 0.167$. We cannot access the lower temperatures for $\Delta = 0.167$ because the system crystallizes. The temperature $T^*$ for each $\Delta$ is listed in table 1. We find that $T^*$ shifts to lower temperatures with decreasing $\Delta$ (increasing the density).
Contrary to the distinct peaks of the specific heat, the FS crossover is harder to detect in the simulation data. Due to the limited range of the temperature in the Arrhenius plot of figure 6, one hardly observes any sort of distinct crossover. In this figure, we marked the temperatures at which the peak of the specific heat are observed with the empty symbols as a guide for the eyes. For the data of $\Delta = 2.667$ and 6, it is not impossible to fit the data of $\tau_\alpha$ with the Arrhenius and super-Arrhenius laws on the low and high temperature sides across $T^*$, but the fitting range is too narrow to call it convincing. Similar fitting was also possible for smaller values of $\Delta$’s, but it is less trustworthy. Therefore, it would be fair to say that the existence of the correlation between the FS crossover and the peak of the specific heat is not conclusive in current numerical simulations [83, 84, 86]. More extensive simulations are required to clarify the relation between the FS crossover and the specific heat peak.

4. Summary and discussion

We have numerically investigated the CP model by tuning the depth of the potential $\Delta$. Changing $\Delta$ corresponds to changing the density of the system. This approach has enabled us to perform simulations over a wide range of densities from the order of unity up to infinity. From the radial distribution functions, the coordination numbers, and the static structure factors, we found that the anisotropic tetrahedral network structures are broken and then the isotropic structures are formed by decreasing $\Delta$ (or increasing the density). We have also calculated various dynamical quantities such as the relaxation time and diffusion constant. These calculations have revealed that their temperature dependence seamlessly changes from Arrhenius to super-Arrhenius behavior. We also confirmed that the temperature dependence of the dynamics is not collapsed by the DT scaling, assuring us that the observed fragility change is not a consequence of the trivial density scaling but is due to the generic change of the mechanism of the glassy dynamics. We have studied the relationship between the fragility and two dynamical quantities, the magnitude of the SE violation and the stretch...
exponent of the density correlation function. The magnitude of the SE violation, which is believed to be a manifestation of the dynamical heterogeneities, correlates well with the fragility of the CP model. On the contrary, the clear correlation between fragility and the stretch exponent has not been observed. Finally, the peak of the specific heat and the possible correlation with the FS crossover have been argued. The peak has been observed in the temperature dependence of the specific heat for most $\Delta$’s in the CP model. In addition, its peak position shifts to lower temperatures with a decrease in the potential depth $\Delta$ (or an increase in density). These observations are related to the recent numerical results obtained in the BKS model [83, 84, 86]. However, it was difficult to identify the FS crossover temperature from the relaxation times because the simulation time windows are too narrow and we conclude that the correlation between the FS crossover and thermodynamic anomaly is still elusive. Further numerical investigation is required.

We address the fact that the CP model exhibits a very broad variation of the fragility, the highest and lowest values of which are comparable to those of the most fragile and strongest liquids studied numerically in the past, and that it can serve as an ideal benchmark for the numerical study of fragility. Note that the harmonic sphere model also shows a very wide variation of the fragility as the density is varied [33, 87]. This model also does not satisfy the DT scaling. However, it should be emphasized that this model is qualitatively different from the CP model. In the harmonic sphere model, the potential is truncated at a certain cutoff distance. At low densities, the model becomes effectively a hard sphere system. Therefore, the temperature and energy are not relevant but, instead, the pressure or density become the controlling thermodynamic parameters. This means that at low densities the temperature dependence of the relaxation time is trivially Arrhenius, whereas at higher densities, the temperature plays a pivotal role, leading to more diverging (or fragile) behavior. For the CP model, on the contrary, the temperature plays a role as a relevant control parameter for all densities and the fragility is continuously controlled.

There are other physical quantities that are expected to be related to fragility [2]: the excess entropy [3], the elastic constants [4, 5], the non-ergodicity parameter [88], the boson peak frequency [5], and the temperature dependence of the microscopic structure [89]. In addition, the relationship between the fragility and the dynamical heterogeneities is a topic which has attracted much attention recently [58, 90, 91]. The comprehensive information on the correlation of these properties with fragility will be obtained from the systematic study of the CP model by tuning a single parameter $\Delta$. Further investigations along this line are currently underway.

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