DO CLOUD–CLOUD COLLISIONS TRIGGER HIGH-MASS STAR FORMATION? I. SMALL CLOUD COLLISIONS

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ABSTRACT

We performed sub-parsec (~0.06 pc) scale simulations of two idealized molecular clouds with different masses undergoing a collision. Gas clumps with densities greater than $10^{-20}$ g cm$^{-3}$ ($0.3 \times 10^4$ cm$^{-3}$) were identified as pre-stellar cores and tracked throughout the simulation. The colliding system showed a partial gas arc morphology with core formation in the oblique shock front at the collision interface. These characteristics support NANTEN observations of objects suspected to be colliding giant molecular clouds (GMCs). We investigated the effect of turbulence and collision speed on the resulting core population and compared the cumulative mass distribution to cores in observed GMCs. Our results suggest that a faster relative velocity increases the number of cores formed but that cores grow via accretion predominately while in the shock front, leading to a slower shock being more important for core growth. The core masses obey a power-law relation with index $\gamma = -1.6$, in good agreement with observations. This suggests that core production through collisions should follow a similar mass distribution as quiescent formation, albeit at a higher mass range. If cores can be supported against collapse during their growth, then the estimated ram pressure from gas infall is of the right order to counter the radiation pressure and form a star of 100 $M_{\odot}$.

Key words: galaxies: ISM – ISM: clouds – ISM: structure – methods: numerical – stars: formation

Online-only material: color figures

1. INTRODUCTION

The role of collisions between the dense clouds of gas in the interstellar medium has flitted on the outside of mainstream star formation theories for over three decades (e.g., Loren 1976). While it is not disputed that such events occur, it has been hard to pin down their frequency and what impact these encounters have on their host galaxy’s star formation rate (SFR). These problems stem from the difficulty in observing both the collision process itself and its most likely products, high-mass stars.

The formation process involving the largest members of the stellar population remains one of a number of diverse theoretical candidates. While low-mass stars can form via accreting gas onto a gravitationally collapsed core (e.g., Palla & Stahler 2002), the evolution of pre-stellar cores and tracked throughout the simulation. The colliding system showed a partial gas arc morphology with core formation in the oblique shock front at the collision interface. These characteristics support NANTEN observations of objects suspected to be colliding giant molecular clouds (GMCs). We investigated the effect of turbulence and collision speed on the resulting core population and compared the cumulative mass distribution to cores in observed GMCs. Our results suggest that a faster relative velocity increases the number of cores formed but that cores grow via accretion predominately while in the shock front, leading to a slower shock being more important for core growth. The core masses obey a power-law relation with index $\gamma = -1.6$, in good agreement with observations. This suggests that core production through collisions should follow a similar mass distribution as quiescent formation, albeit at a higher mass range. If cores can be supported against collapse during their growth, then the estimated ram pressure from gas infall is of the right order to counter the radiation pressure and form a star of 100 $M_{\odot}$.

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1. INTRODUCTION

The formation process involving the largest members of the stellar population remains one of a number of diverse theoretical candidates. While low-mass stars can form via accreting gas onto a gravitationally collapsed core (e.g., Palla & Stahler 2002; Shu et al. 1987), this process most likely fails in the case of a massive star due to both the timescales involved to accrete sufficient mass and the radiation pressure and ionization that the growing core would produce, thereby stopping the accretion before a large enough object is formed. To counter these problems, the proposed models either modify the physical conditions of the accretion via such mechanisms as dust content (Wolfire & Cassinelli 1987), wind blown cavities (Krumholz et al. 2005), and accretion disks (Yorke & Sonnhalter 2002) or opt for later evolution with physical collisions between low-mass stars (Bonnell et al. 1998). In their paper, McKee & Tan (2002) propose that such problems can be avoided if the collapsed core is turbulent and the surface density is sufficiently high with $\Sigma > 0.5$ g cm$^{-2}$ needed for a 100 $M_{\odot}$ star. In such cases, the ram pressure associated with accretion exceeds the radiation pressure.

The creation of the higher surface densities required by McKee & Tan (2002) is a point in favor for cloud–cloud collisions. In this process, interstellar clouds moving at supersonic velocities collide and produce a shock wave at the collision interface. Where the shock compresses the cloud gas, the densities rise and clumps in the post-shocked gas collapse under the effect of enhanced self-gravity (e.g., Stone 1970; Gilden 1984). Since clouds moving at the required supersonic velocities are readily observed (Rosolowsky et al. 2003; Bolatto et al. 2008; Heyer et al. 2009) and both the interstellar medium and the star-forming giant molecular clouds (GMCs) are known to be turbulent (Larson 1981; Elmegreen 2002; Mac Low & Klessen 2004), this dynamic picture of triggered core formation has many points in its favor compared to a quasi-static viewpoint.

1.1. Observational Evidence for Cloud–Cloud Collisions

Examples of probable cloud–cloud collisions are steadily increasing. In such cases, observations identify two distinct velocity components in the gas, belonging to the two clouds undergoing a collision. Early observations of this phenomenon include Loren (1976, 1977), who identified two components in the CO spectra of the molecular cloud NGC 133 which they propose is the cause of the chain of newly formed stars within the cloud, and later in LkHα 198, a molecular cloud containing Herbig Be/Ae stars. Dickel et al. (1978) also found two velocity components in Dr21/W75 (a high-mass star-forming region) and Odenwald et al. (1992) attributes the star formation and elongated shape of the unbound high-altitude cloud GR110-13 to compression during a cloud collision.

More recent observations include the two super star clusters Westerlund 2 and NGC 3603. Super star clusters are tightly packed stellar groups with radii ~1 pc and masses ~$10^4$ $M_{\odot}$ which contain a large number of massive stars. Their formation has historically perplexed researchers due to the problem of creating such a high-mass cluster if the star formation efficiency inside the GMC is low. The first cluster to be identified as a possible collision object was Westerlund 2, which was observed by Furukawa et al. (2009) and Ohama et al. (2010) and found to have two associated clouds with relative velocity of 20 km s$^{-1}$. The authors propose that the resulting shock between the clouds compressed the gas to produce the massive

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A. Ohama et al. (in preparation) later identified two GMCs associated with NGC 3603, prompting suggestions that it could have a similar formation mechanism. A third recent cloud collision candidate was found in observations of the Galactic H II region Trifid Nebula, M20, performed by Torii (2011). They identified two clouds with masses of $10^3 M_\odot$ and relative velocity $10 \text{ km s}^{-1}$ moving toward a central O star in M20 and suggest this object was created during the clouds’ collision. Notably, the relative velocities observed in these three events are too high for the clouds to be gravitationally bound to one another, supporting the idea that these are examples of accidental collisions.

Despite the increasing frequency of observations, the total number of cloud collision candidates remains small, suggesting that such triggered star formation is indeed a minor addition to the Galaxy’s total SFR. However, new observations using NANTEN2/NANTEN 4 m sub-millimeter/millimeter telescope conversely suggest that such events have previously been misclassified and are significantly more numerous that previously thought. K. Torii et al. (in preparation) argue that the ring structure seen in the Galactic H II region, RCW120, is a classic example of what is expected in a cloud collision. RCW120 is one of the Spitzer bubbles (Churchwell et al. 2006): a collection of 322 objects, 52 of which show a similar ring morphology. This distinctive shape has previously been accounted for using the wind-blown model (Castor et al. 1975; Weaver et al. 1977), whereby stellar winds from a central high-mass star cause gas to be swept into a spherical shell. However, bubbles such as RCW120 display partial arcs rather than complete rings with high dust concentration on the outer edge of the ring instead of the interior. The star formation is also off-center, pointing toward a bow shock rather than formation via internal expansion.

1.2. Theoretical Models of Cloud–Cloud Collisions

The idea that such a morphology is the product of cloud collisions is further supported by theoretical calculations. Habe & Ohta (1992) performed two-dimensional simulations of a head-on collision between non-identical clouds. They found that the larger cloud was disrupted by the resulting bow shock which, in turn, compressed the smaller cloud. This compression caused the post-shock gas in the smaller cloud to become gravitationally unstable, even in the case where the cloud was initially below its Jeans mass. The geometric structure of the collision shows the same ring-like morphology as seen in the Spitzer bubbles, with dense cores for the expected star formation forming in the compressed shock, not in the center of the ring.

Anathpindika (2010) performed a similar simulation where they looked at the stability of the post-collision bow shock in three-dimensional simulations. While initially supported by turbulence, shocks within the bow shock cause it to be susceptible to a number of hydrodynamic instabilities including the Kelvin–Helmholtz instability between shearing fluids, the Rayleigh–Taylor buoyancy instability, and the thin shell instability which occurs when a shocked shell of gas becomes unstable to small perturbations, developing expanding ripples. Of these three, the thin shell instability was deemed the most important for bow-shock evolution, causing it to bend at the apex and extend along the collision axis in a filament that fragments to form cores. The creation of such a structure was proposed to be the origin for filament-type clouds, such as the Orion molecular cloud.

Anathpindika (2010) also note the importance of the relative collision speed between the clouds, finding that a relative velocity of $20 \text{ km s}^{-1}$ produced cores with masses between $25–30 M_\odot$ in clouds of mass $5000 M_\odot$ and $2000 M_\odot$, whereas a lower velocity of $\sim 5 \text{ km s}^{-1}$ failed to produce any cores. This finding was further supported by colliding flow simulations of magnetized non-homogeneous gas by Inoue & Fukui (2013). They found the mass of the generated core depended on both this collision velocity and the strength of the initial magnetic field.

On a larger scale, Tasker & Tan (2009) and Tasker (2011) have tackled the problem of how common accidental collisions between clouds are likely to be. They find that in a simulation of a Milky Way-type disk, multiple collisions can occur per an orbital period, with a rate of approximately five per an orbit. This agrees with analytical calculations performed by Tan (2000), who argues that if the rate of collisions is enough to achieve multiple encounters per an orbital period, then cloud collisions could drive the SFR in the galaxy, producing the empirical Kennicutt–Schmidt relation between gas surface density and SFR (Kennicutt 1998).

In this paper, we examine the formation of dense, star-forming cores in a head-on cloud–cloud collision between non-identical clouds and investigate the impact of turbulence and collision speed on the properties and evolution of these cores. Section 2 describes the details of our simulation, Section 3 looks at the effect of turbulence, Section 4 explores the collision speed, and in Section 5 we present our conclusions.

2. NUMERICAL METHODS

Our simulations were run with Enzo: a three-dimensional hydrodynamical adaptive mesh refinement code (The Enzo Collaboration et al. 2014; Bryan 1999; Bryan & Norman 1997). We used a box size of side 30 pc with a top level root grid size of $128 \times 128 \times 128$ and an additional two levels of refinement, giving a limiting resolution (smallest cell size) of $\sim 0.06 \text{ pc}$. The refinement criteria were based on baryon mass and the resolution of the Jeans length, which must be refined by at least four cells, as suggested by Truelove et al. (1997).

The hydrodynamics were evolved over time using a three-dimensional implementation of the Zeus astrophysical code (Stone & Norman 1992). To handle shocks, Zeus uses an artificial viscosity where the associated variable, the quadratic artificial viscosity term, is set to 2.0 (the default value).

Gas cools radiatively down to 10 K using a one-dimensional cooling table created using the CLOUDY cooling code (Ferland et al. 1998) where solar metallicity and a density of 100 cm$^{-3}$ were assumed. For the densities achieved in our simulation, the cooling function remains relatively constant, allowing us to use this simplification.

In order to prevent gas undergoing unrefined collapse on the finest grid level, we impose a pressure floor. In a collapsing region where the Jeans length can no longer be refined by the desired four cells, the pressure is increased so that the gas follows a polytrope with an adiabatic index $\gamma = 2.0$. This polytrope is stable and stops the collapse at a finite density, preventing single cells from becoming impossibly dense compared to their surroundings as gravitationally unstable gas flows toward their center.

While the Truelove limit of four cells per Jeans length is designed to prevent spurious fragmentation, it may not be sufficient to resolve the turbulence on the smallest scales. In simulations performed by Federrath et al. (2011), 30 cells per Jeans length were required to converge the values of the turbulent energy. In our current simulations, this cell number
corresponds to a physical length greater than our core size. We therefore note that while the overall fragmentation of the gas into star-forming regions is correctly followed, the velocity dispersion within these cores is unlikely to have reached a converged value. However, since the primary questions in this paper focus on the formation of potential star-forming sites, this limit is sufficient to assess the impact of the cloud collision. To confirm this, in Section 5 we compare our results with a simulation performed at twice the resolution.

A point related to the above is the impact of the pressure floor on the dense cores. The increased pressure at our maximum refinement prevents unresolved collapse but also impacts the evolution of the internal core properties. An alternative technique would have been to utilize sink particles which estimate an accretion rate according to the surrounding density and temperature when the gas reaches a high density and meets additional criteria that identify bound and collapsing regions (e.g., Federrath et al. 2010); however, considering where our resolution becomes limited and the difficulty involved with destroying a sink, we chose to keep the cores as pressure-supported gas, but note that this introduces an error in their internal values.

2.1. Core Identification and Tracking

Star-forming cores are identified in the simulation via a constant density contour finding algorithm (Turk et al. 2011). In the majority of our results, this density threshold is set to $\rho_{\text{crit}} = 10^{-20} \, \text{g cm}^{-3}$, although we also compare the evolution in core number with core selection at $\rho_{\text{crit}} = 10^{-19} \, \text{g cm}^{-3}$ and $\rho_{\text{crit}} = 5 \times 10^{-21} \, \text{g cm}^{-3}$ in Section 4.5.1. In comparison, the average GMC density is observed to be $\sim 100 \, \text{cm}^{-3}$ while star formation is seen to occur at $10^4 \, \text{cm}^{-3} \simeq 3 \times 10^{-20} \, \text{g cm}^{-3}$ (observations by Ginsburg et al. 2012; Lada et al. 2010 and theoretical estimate from Padoan et al. 2013). Therefore, within these cores, gravity is likely to dominate over other physical processes to result in star formation.

In order to analyze the evolution of the core properties, we track their motion over the time of the simulation. This process is performed in a similar manner to the cloud tracking scheme presented in Tasker & Tan (2009) and works as follows.

1. Data outputs are taken at 0.1 Myr intervals during the simulation and cores are identified via the above criteria in all outputs.

2. The position of each core is predicted in the next time step via $r_{c,t} = r_{c,t-1} + v_{c,t-1} \Delta t$, where $r_{c,t}$ is the core position at time $t$, $r_{c,t-1}$ and $v_{c,t-1}$ are the core position and velocity one output earlier, and $\Delta t$ is the time passed between outputs, 0.1 Myr.

3. A spherical volume of radius $2 v_{c,t-1} \Delta t$ is searched around each predicted position for cores present in the time, $t$, output. The closest core in that region is assumed to be the same core 0.1 Myr later. If no cores are found, then the core is assumed to have dissipated or merged with another core.

4. In the case of two cores being assigned to the same present-time core, the closest one is tracked.

An example of core tracking is shown for three times at 0.1 Myr intervals in Figure 1. The surface density of a 4 pc section of the shock front during a collision with a relative velocity of 5 km s$^{-1}$ is imaged with the core positions and their assigned number overlaid. It is possible to confirm by eye whether or not cores found in equivalent positions as the shock progresses maintain the same tracking number.

3. THE INITIAL CONDITIONS

The simulation initial conditions consist of two clouds of unequal masses whose boundaries are separated by approximately 1.2 pc, as shown in Figure 2. The density distribution of each cloud takes the form of a Bonner–Ebert sphere (Bonnor 1956); a hydrostatic isothermal self-gravitating gas sphere that is confined by its external pressure. The maximum mass such a sphere can have and remain stable is given by

$$M_{\text{BE}} = \frac{c_{\text{BE}} c_s^4}{P_{\text{ext}}^{1/2} G^{3/2}},$$

(1)

where $c_s$ is the isothermal sound speed, $c_{\text{BE}} = 1.18$ is a constant, $P_{\text{ext}} = 4000 \times k_B$ ($k_B$: Boltzmann constant) is the external gas pressure, and $G$ is the gravitational constant. Both the simulated clouds fulfill this stability requirement, having masses of 417 $M_\odot$ and 1635 $M_\odot$, both equivalent to 0.43 $M_{\text{BE}}$ at 120 K and 240 K, respectively. Their properties are detailed more fully in Table 1. Once cooling begins, the cloud becomes unstable and without additional support will start to collapse.

This profile was primarily chosen because the initial stability is appealing when considering the impact of outside effects.
Figure 2. Surface density of the initial conditions. Both spheres have a Bonnor–Ebert density profile and constant temperature. When turbulence is included, the velocity field is perturbed as described in Section 3.

(A color version of this figure is available in the online journal.)

Table 1

| Cloud Parameters | Cloud 1 | Cloud 2 |
|------------------|---------|---------|
| $T_{BE}$ (K)     | 120     | 240     |
| $t_f$ (Myr)      | 5.31    | 7.29    |
| $r_f$ (pc)       | 3.5     | 7.2     |
| $M_c$ ($M_\odot$) | 417   | 1635    |
| $\sigma_v$ (km s$^{-1}$) | 1.25 | 1.71 |
| $\bar{n}$ (cm$^{-3}$) | 47.4  | 25.3    |
| $k$ mode         | 6–12    | 10–25   |

Note. From top to bottom: temperature, free-fall time, radius, mass, velocity dispersion, average density, and initial $k$ mode used when turbulence is included.

However, molecular clouds have also been observed to show a Bonnor–Ebert density profile in the work of Alves et al. (2001). Other clouds, meanwhile, have a higher mass than their Bonnor–Ebert mass, but despite this are not in free-fall collapse due to additional support from internal turbulent motions. This allows $c_s$ in the above equation to be switched for the effective sound speed which also includes a contribution from the velocity dispersion.

Compared to observed GMCs, the cloud mass we have selected is small. Typical clouds within the Milky Way have masses $\sim 10^4$–$10^5 M_\odot$ (Heyer et al. 2009), a factor of 10 above our chosen sizes. The results from collisions between larger clouds will be explored in subsequent papers, but selecting a smaller cloud at this stage allows a simpler study of the shock front evolution at high resolutions.

3.1. Turbulence

In simulations where the gas is given an initial turbulence, we impose a velocity field with a power spectrum of $v_k^2 \propto k^{-4}$, corresponding to the expected spectrum given by Larson for GMCs (Mac Low et al. 1998; Larson 1981). To ensure the turbulence modes were adequately resolved, we selected a maximum $k$ mode value of one-tenth of the number of cells across the cloud. In addition, we removed the lower-order modes since these larger-scale perturbations disrupted the cloud structure, causing it to fragment prior to collision. In previous work designed to model turbulence in GMCs, driving on larger scales was found to produce a closer match to observations.

Before considering the cloud–cloud collision, the duration of the clouds’ stability is tested while in situ over the free-fall time of Cloud 1 (see Table 1). This time is longer than the collision duration (as measured by the shock crossing time) for the two faster collision speeds we consider in Section 4.2 and approximately 70% of the collision duration for our slowest collision speed.

This run was performed to differentiate between structural evolution from the collision process and independent changes within the cloud. Figure 3 images the density for the case when turbulence is not included (left) and when it is added to the initial conditions as described in Section 3.1. Without turbulence, the clouds collapse as they cool within the expected free-fall time. After 5.3 Myr, one free-fall time for Cloud 1 has passed and its radius has contracted to the dense point shown at $x = -7$ pc in Figure 3. When turbulence is included, the cloud is supported against cooling over the same duration.

In the left-hand panel of Figure 3, four dense lines are seen like compass points on Cloud 2 as it collapses. These have the
hallmarks of a numerical artifact and are due to a preferential grid alignment in the fluid instabilities. As the gas cools, the cloud’s internal energy decreases and pressure equilibrium is broken. As the innermost region of the cloud begins to collapse, the background gas presses down on the surface layer, creating a dense outer ring which becomes unstable to gravitational collapse by turbulence, as described in Section 3.1, and collide with velocities of 3 km s$^{-1}$ (3CC), 5 km s$^{-1}$ (5CC), and 10 km s$^{-1}$ (10CC). The final simulation repeats the 5 km s$^{-1}$ event at higher resolution (5CCHR). A summary of these runs is given in Table 2. In the values listed in the table, $t_{\text{cross}}$ and $t_{\text{cross}}$ are the times for the shock to pass through Cloud 1 and Cloud 2, respectively, after contact. Both these and the shock speed are measured by plotting the shock progression in the density along a line of sight directed along the collision axis.

4. RESULTS

The collision between Cloud 1 and Cloud 2 in Table 1 was performed under a variety of different conditions. In the first simulation (noTurb), the clouds were given no internal turbulence and collide with a relative velocity of 3 km s$^{-1}$. The next three simulations begin with the clouds supported against gravitational collapse by turbulence, as described in Section 3.1, and collide with velocities of 3 km s$^{-1}$ (3CC), 5 km s$^{-1}$ (5CC), and 10 km s$^{-1}$ (10CC). The final simulation repeats the 5 km s$^{-1}$ event at higher resolution (5CCHR). A summary of these runs is given in Table 2. In the values listed in the table, $t_{\text{cross}}$ and $t_{\text{cross}}$ are the times for the shock to pass through Cloud 1 and Cloud 2, respectively, after contact. Both these and the shock speed are measured by plotting the shock progression in the density along a line of sight directed along the collision axis.

4.1. Non-turbulent Collision

Figure 5 shows density slices from the cloud collision without initial internal turbulence at $t = 1.4$ Myr (left) and 3.9 Myr. The relative velocity of the clouds is 3.0 km s$^{-1}$. In the left-hand panel, the clouds are shown at the early stage of the collision with their boundaries having just begun to touch. By this point, the clouds have cooled to a gas temperature of 10 K (the lower limit of our cooling curve), reducing the internal gas pressure and causing the clouds to begin gravitational collapse from their own self-gravity. The outer rims of the clouds are compressed by the external gas pressure, forming thin, compressed gas shells at their surface. The shells themselves show a small, irregular ripple structure due to the Rayleigh–Taylor buoyancy instability triggered by their lower-density surroundings.

Strong shock waves appear at the interface between the clouds, forming a thin, dense disk of shocked gas. Within this disk, the ripple structure in the thin surface shells is enhanced due to the thin shell instability, with the thin shell being bounded

![Figure 4](image_url)
on both sides by the progressing shocks from the collision and accelerated by Cloud 1’s continual motion.

Since it has the higher density, Cloud 1 starts to penetrate the larger Cloud 2, producing an oblique shock front that presses on the concave region of the thin disk, increasing the gas surface density and continuing to push down. Meanwhile, the shockwave entering Cloud 2 becomes a bent bow shock. This can be seen clearly in the right-hand panel of Figure 5, which shows the collision at the later stage of \( t = 3.9 \) Myr. By this time, the shocked thin disk has laterally contracted due to its own self-gravity to form a bound dense core at its center. This result agrees well with the previous two-dimensional study performed by Habe & Ohta (1992), who also found that due to the size difference between the two clouds, the shock wave entering the larger cloud forms a bow shock. At its apex, the smaller cloud’s post-shocked gas is compressed into a disk which collapses under self-gravity to form a single dense core. This core continues to move through the larger cloud, which simultaneously continues to contract under gravity.

The formation of the bound core occurs at 3.9 Myr, considerably shorter than Cloud 1’s free-fall time of \( t_{\text{ff1}} = 5.31 \) Myr. The collision process therefore enhances the gravitational instability of the cloud. Since the entire cloud is compressed into this core, its mass is equal to that of Cloud 1.

### 4.2. The Effect of Varying Collision Velocity

We move on to exploring the effect of the clouds’ relative collision speed on the properties of the cores formed during the interaction. The three simulations presented in this section all use turbulence to initialize Cloud 1 and Cloud 2, which collide with relative velocities of 3 km s\(^{-1}\), 5 km s\(^{-1}\), and 10 km s\(^{-1}\).

As described in Section 3.1, the clouds remain stationary for 0.5 Myr to allow the development of their internal turbulent structure, after which point Cloud 1 begins to move toward the stationary Cloud 2.

The evolution of these three simulations is shown in Figure 6, with the time progressing from left to right. Each image shows the surface density averaged over a depth of 0.2 pc. The top row of three panels shows the evolution of the simulation with a relative cloud collision speed of 3.0 km s\(^{-1}\), the middle row shows the results using a collision speed of 5.0 km s\(^{-1}\), while the bottom row shows the final tested speed of 10 km s\(^{-1}\). The times shown correspond to the same event in each simulation: the panels furthest to the left show the time of the first core formation (3.0, 1.6, and 0.9 Myr, respectively, for the 3 km s\(^{-1}\), 5 km s\(^{-1}\), and 10 km s\(^{-1}\) simulation after the runs begin), the middle panel shows the time when there exists the maximum number of cores (4.6, 3.7, and 2.2 Myr), and the final right-hand panel shows the clouds as the shock exits Cloud 2 (6.5, 5.2, and 2.8 Myr).

In all three cases, the initial progression of the shock formed in the collision is the same: since the relative velocities of the colliding clouds are supersonic, isothermal shock waves appear in both clouds, as was seen in Section 4.1 for the non-turbulent collision case. However, since the pre-shocked gas in the clouds now has a filamentary structure formed from via turbulence, the propagation of the shock becomes more complicated.

In Figure 7, we show an alternative simulation to the main ones presented in this section. The relative velocity between the two colliding clouds is 10 km s\(^{-1}\), but unlike our previous 10 km s\(^{-1}\) case, both the clouds move with velocities of 5 km s\(^{-1}\) and −5 km s\(^{-1}\). The results from this are identical to those for Cloud 1 moving with 10 km s\(^{-1}\), but the shape of the shock front is now starkly visible in the magnitude of the gas velocity that is shown in Figure 7. In the left-hand panel, the velocity magnitude is shown at an early stage in the collision at \( t = 0.8 \) Myr after the beginning of the simulation. The gas filaments formed by the turbulence lie at a range of angles to the collision axis, creating a shocked interface at the cloud contact point that is not straight but follows these oblique angles. As with the thin disk previously seen in Section 4.1, ripples are formed along the shocked filaments with a spatial scale much smaller than the filament length. These ripples are then enhanced by the thin shell instability.

As Cloud 1 penetrates the larger Cloud 2, the oblique arc of the overall shock front focuses on the concave parts of the shocked filaments and increases their mass and density. These sections begin to gain inertia, causing them to slow with respect to the shock front and creating a displacement that increases with time. This can be seen in the right panel of Figure 7.

### 4.3. One-dimensional Density Distributions

After the initial formation of the oblique shock front, the colliding clouds take on visually different forms depending on their relative collision velocity. In the middle and bottom panels of Figure 6, the combined gas from the colliding clouds forms an open arc that is marked more strongly in the higher-velocity collisions. This distinctive shape resembles the observations...
performed by K. Torii et al. (in preparation) of the Galactic H II region, RCW120, which they postulate is the result of a cloud collision. At the final time shown, dense structures can be seen in the 3.0 km s\(^{-1}\) and 5.0 km s\(^{-1}\) case, but gas remains at a lower density in the 10 km s\(^{-1}\) simulation.

The overall gas density of the clouds can be explored in the one-dimensional probability distribution functions (PDFs) shown in Figure 8 for the non-collision case and the three different collision velocities considered. Gas is included in the PDF if it is within a 7 pc radius sphere centered on Cloud 2. The blue dashed line in all of the panels marks a log-normal profile with the following equation:

\[
f(x; \mu, \sigma) = \frac{A}{\sigma \sqrt{2\pi}} e^{-\frac{1}{2} \left(\frac{x-\mu}{\sigma}\right)^2},
\]

where \(x = \ln \rho/\bar{\rho}\) and the constants have values of \(A \sim 1.2\), \(\mu \sim -0.3\), and \(\sigma = 0.9\).

In the top left panel of Figure 8, the static evolution of Cloud 2 is shown without any collision event. The black solid line shows the gas at 1.0 Myr and the red dotted line shows the profile after the free-fall time of the smaller Cloud 1, \(t_{\text{ff1}} = 5.3\) Myr: the duration of that simulation and longer than the shock crossing time in either the 5.0 km s\(^{-1}\) or 10 km s\(^{-1}\) case. In the static cloud simulation, the gas above a density of 10.0 cm\(^{-3}\) closely follows a log-normal distribution throughout the simulation. At lower densities, background gas from around the cloud forms a peak at \(\sim 0.5\) cm\(^{-3}\).

However, the next three plots show clear deviations in that higher-density region. The top right panel shows the result for the 3.0 km s\(^{-1}\) case while on the bottom row the left-hand panel
Figure 8. Probability distribution functions (PDFs) for the cloud collisions at different relative velocities. The blue dashed line shows a log-normal fit. The top left shows the comparison static case for the gas in Cloud 2 when it does not undergo a collision. The black solid line depicts the profile at 1.0 Myr while the red dotted line is the gas at \( t_{\text{ff1}} = 5.3 \) Myr. The high-density gas maintains a log-normal fit over the duration of the simulation. The top right shows the result for the 3.0 km s\(^{-1}\) collision case, the bottom left the 5.0 km s\(^{-1}\) case, and the bottom right the 10.0 km s\(^{-1}\) simulation. In all three cases, the black solid line shows the profile when the maximum number of cores are present. Upon forming the cores, the gas deviates from the log-normal to grow an extended tail.

(A color version of this figure is available in the online journal.)

This result—deviation from the log-normal is linked with star formation—agrees strongly with the observations from Kainulainen et al. (2009), who found that GMCs without active star formation show a log-normal distribution, while clouds displaying star formation show prominent non-log-normal wings. This result was also found in simulations by Federrath & Klessen (2013), who modeled the evolution of a periodic box of isothermal star-forming gas under a variety of different conditions for turbulent driving and magnetic fields. They found that the PDF developed a tail in all of the cases where the star formation efficiency was not zero.

A related result was found by Tremblin et al. (2014), who found a double PDF structure in clouds containing an expanding H\(\text{II}\) region. They concluded that this was a signature of triggered star formation, with an additional power-law tail due to the gravitational effects. Such a double PDF structure would support the extended tail in Figure 8, although the second peak is not strongly visible.

4.4. Turbulence Characterization

The shape of the PDFs can be directly related to the type of turbulence inside the cloud. For an isothermal gas, the width of the PDF grows with increasing Mach number where the value of the proportionality constant is determined by the modes of turbulence present (Federrath et al. 2008; Passot & Vázquez-Semadeni 1998). Since the majority of the cloud gas sits close to the bottom end of our cooling curve at 10 K, we can apply the relation for a non-magnetized gas between these three quantities (Burkhart & Lazarian 2012; Padoan et al. 1997):

\[
\sigma_s^2 = \ln(1 + b^2 M^2),
\]  

(3)

where the width of the PDF is determined by the logarithmic standard deviation, \( \sigma_s \), in \( s \equiv \ln(\rho/\bar{\rho}) \), the natural logarithm of the density divided by the mean density. The cloud Mach
number is defined as $M \equiv \sigma_{3D}/c_s >$ for the speed of sound, $c_s$, and three-dimensional velocity dispersion, $\sigma_{3D}$.

In simulations performed by Federrath et al. (2008), the value of the proportionality term, $b$, was found to be dictated by how the turbulence was being driven. When compressive forcing was used in their calculations, the standard deviation was three times larger than with solenoidal (divergence-free) forcing. The former gave a value of $b \sim 1$, while solenoidal turbulence produced $b \sim 1/3$.

Rearranging Equation (3) for $b$ gives $b = \sqrt{\text{exp}(\sigma^2) - 1}/M^2$, which is plotted in Figure 9 for Cloud 2 over the duration of the simulation. As with the PDF plots in Figure 8, gas is included in the calculation for $b$ if it is within a 7 pc radius sphere centered on Cloud 2. The solid black line shows the static evolution of Cloud 2 in the absence of any collision, while the green dot-dash line shows the results for the 3 km s$^{-1}$ collision, the blue dashed line marks the 5 km s$^{-1}$ evolution, and the red dotted line is for the 10 km s$^{-1}$ run. In all cases, the turbulence is injected into the equilibrated sphere at $t/t_{\text{ff1}} = 0$, which begins to cool, lowering the sound speed and causing $b$ to drop. As the turbulence begins to decay, the velocity dispersion decreases and $b$ rises. At the point where Cloud 1 begins to move and the internal density structure of both clouds has reached the log-normal profile seen in Figure 8, $t/t_{\text{ff1}} = 0.1$ and $b \sim 0.5$, suggesting a mix of compressional and solenoidal modes in the filamentary structure created by the turbulence.

In the absence of a collision, the Mach number and density standard deviation tend toward roughly constant values to form the weakly filamentary structure shown in the right-hand panel of Figure 3. This corresponds to a steady $b$ value of around 0.7. In the case of a collision, the velocity dispersion and Mach number initially rise as Cloud 1’s material meets Cloud 2. This first contact is prior to the shock forming, so the standard deviation in density remains unchanged, causing the value of $b$ to drop. As Cloud 1 penetrates Cloud 2, the shock front forms with an accompanying jump in the density deviation. This occurs at $t/t_{\text{ff1}} \approx 0.38, 0.28,$ and 0.19 for the 3 km s$^{-1}$, 5 km s$^{-1}$, and 10 km s$^{-1}$ cases, respectively. The density within the shock front continues to grow as Cloud 1 pushes forward and the $b$ value turns and begins to increase, driving into the compressional regime. This turning point occurs most rapidly after the clouds touch in the 10 km s$^{-1}$ case, since the stronger shock raises the density standard deviation most quickly. In the case of the 3 km s$^{-1}$ and 5 km s$^{-1}$ runs, the density standard deviation continues to grow and $b$ escalates. We will see in the next section that this rapid increase in $b$ corresponds to the formation of a gravitationally bound core, whose mass undergoes runaway growth. The 10 km s$^{-1}$ collision begins this process but the shock wave exits the cloud before the density standard deviation gets very high. This rapid progression will actually turn out to prevent a bound core from forming.

As described in the previous section, from both observations and simulations, the shape of the density PDF is associated with the cloud’s star formation. Since the width of the PDF depends on $b$, this association can be carried through to explore the link between star formation and turbulence type. In their paper, Federrath & Klessen (2012) derived the $b$ dependence from six analytical star formation models that are based on the density PDF. They found that $b$ positively correlated with star formation efficiency, which they ascribed to the compressional modes being more effective at forming more dense star-forming regions. Our results support this conclusion with the formation of the shock front corresponding to a marked rise in $b$ which takes it into the compressional regime. This then forms cores which become gravitationally bound and collapse, causing self-gravity to dominate the density field over turbulence and escalating the value for $b$.

4.5. Core Formation

As described in Section 2.1, gas which has the potential for star formation is defined as a “core” when it reaches a threshold density of $\rho_{\text{thresh}} = 10^{-20}$ g cm$^{-3}$. Using this definition and the tracking described in the same section, we identified the cores in the three simulations and explored their properties.

4.5.1. Core Number Evolution

Unlike when turbulence was not included in Section 4.1, multiple cores with densities higher than our core threshold, $\rho_{\text{thresh}} = 10^{-20}$ g cm$^{-3}$, are formed in all three runs performed at different collisional velocities. The evolution of the core number plotted as a fraction of Cloud 1’s free-fall time is shown in Figure 10 until 1.0 Myr after the shock exits Cloud 2. From left to right, the figure shows the core evolution for the runs with collisional velocity of 3 km s$^{-1}$, 5 km s$^{-1}$, and 10 km s$^{-1}$. The initial time in the plots, $t = 0$, corresponds to the clouds just prior to collision as their surfaces touch. Each plot considers four different density values for the core definition to provide a quantitative feel for the fragmentation of the gas:

- $\rho = 5 \times 10^{-21}$ g cm$^{-3}$ (black solid line), $\rho_{\text{thresh}} = 10^{-20}$ g cm$^{-3}$ (red dashed line), $\rho = 5 \times 10^{-20}$ g cm$^{-3}$ (dotted line), and $\rho = 10^{-19}$ g cm$^{-3}$ (blue chain line). As mentioned in the earlier sections, star formation is observationally seen to occur at densities around $10^4$ cm$^{-3} \approx 3 \times 10^{-20}$ g cm$^{-3}$ (Lada et al. 2010).

In all simulations, core formation at our main threshold density (red dashed) and at the lower-threshold value (black...
gas having less time to grow in density within the shock front, to lower as non-bound cores dissipate. The rate of dissipation is expand and drop in density. This causes the core number to begin maximum core count, with three times as many cores formed thresholds, the increase in velocity also corresponds to a higher we increase the collision speed. In the case of the two lower core populations.

As the shock leaves Cloud 1, the post-shock gas begins to expand and drop in density. This causes the core number to begin lower as non-bound cores dissipate. The rate of dissipation is also related to shock speed with the faster collision resulting in gas having less time to grow in density within the shock front, leading to a more rapid reduction in core number once the shock has passed. In the 3 km s\(^{-1}\) and 5 km s\(^{-1}\) simulations, one bound core is formed that persists through to the end of the simulation.

The need for the shock front to remain in the cloud long enough to allow core growth is seen more clearly when the core threshold density is increased to consider the formation of objects at \(\rho = 5 \times 10^{-20} \text{ g cm}^{-3}\) and \(\rho = 10^{-19} \text{ g cm}^{-3}\), where the previous trends appear to break down when we reach the 10 km s\(^{-1}\) collision. In both the 3 km s\(^{-1}\) and 5 km s\(^{-1}\) cases, higher-density cores are formed after \(t/t_{\text{ff}} = 0.6\) with the formation occurring earlier for the 5 km s\(^{-1}\) simulation in the same pattern as for the lower-density cores. However, in the 10 km s\(^{-1}\) simulation, no cores are seen after \(t/t_{\text{ff}} = 0.5\). At this stage, the faster shock generated in the 10 km s\(^{-1}\) case has passed through Cloud 1 entirely, before the gas has had the chance to reach the higher-density thresholds. With none of the cores formed becoming gravitationally bound, the post-shock gas swiftly drops in density, leaving no gas above any of the considered thresholds.

### 4.5.2. Core Properties

The properties of each of the cores formed in the simulation are shown in Tables 3–5 where we list the five most massive cores. For each core found, the mass, radius, average number density, velocity dispersion, virial parameter, and estimated accretion rate are shown. The core radius is defined from the core volume, \(V_{\text{core}}\), as \(r_{\text{core}} = (3V_{\text{core}}/4\pi)^{1/3}\). The virial parameter, \(\alpha_{\text{vir}}\), is a measure of the ratio of the kinetic and potential energy for a spherical object, defined by

\[
\alpha_{\text{vir}} = \frac{5\sigma_{\text{th}}^2 r_{\text{core}}}{GM},
\]

with \(\sigma_{\text{th}}\), the one-dimensional velocity dispersion of the core, including the sound speed: \(\sigma_{\text{th}} \equiv (c_s^2 + \sigma_{\text{ID}}^2)^{1/2}\). A value of \(\alpha_{\text{vir}} < 1\) implies that the core is virialized with the total kinetic energy of the cloud equaling half its gravitational energy. A gravitationally bound core should correspond to \(\alpha_{\text{vir}} < 2.0\).

Comparing the core properties across the three different collisional velocities, the effect of the shock wave’s duration inside the cloud is once again apparent; the slower the collision, the longer the gas spends inside the shock front, allowing a higher-mass core to be formed. So while the number of cores increases with higher collision speed, the core mass obtained is related to the length of time the shock remains inside the

---

Table 3

| \(M_{\odot}\) | \(r_{\text{core}}\) (pc) | \(\dot{n}\) (cm\(^{-3}\)) | \(\sigma\) (km s\(^{-1}\)) | \(\alpha_{\text{vir}}\) | \(M_{\odot}\) yr\(^{-1}\) |
|----------------|----------------|----------------|----------------|----------------|----------------|
| 47.85          | 0.35           | 2.55E+04       | 0.34           | 1.52           | 4.23E-04       |
| 14.04          | 0.24           | 1.17E+04       | 0.21           | 2.07           | 3.42E-04       |
| 4.35           | 0.18           | 5.93E+03       | 0.13           | 3.59           | 3.40E-05       |
| 3.06           | 0.16           | 5.80E+03       | 0.20           | 6.23           | 2.28E-05       |
| 2.21           | 0.15           | 4.14E+03       | 0.18           | 7.34           | 1.18E-05       |

(A color version of this figure is available in the online journal.)

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Figure 10. Core number evolution as a fraction of Cloud 1’s free-fall time for simulations at three different collision velocities. From left to right, the panels show the 3 km s\(^{-1}\) run, 5 km s\(^{-1}\) run, and 10 km s\(^{-1}\) run. \(t = 0\) corresponds to the time when the clouds are just touching. The lines represent cores formed at different density thresholds. The black solid line is for a core density of \(5 \times 10^{-21} \text{ g cm}^{-3}\). The red dashed line is our usual definition of \(1 \times 10^{-20} \text{ g cm}^{-3}\). The dotted line marks a threshold of \(5 \times 10^{-20} \text{ g cm}^{-3}\) and the blue chain line is at \(1 \times 10^{-19} \text{ g cm}^{-3}\). As the collision velocity increases, the lower-density cores (black solid line and red dashed line) increase in number as the cores form faster. However, in the 10 km s\(^{-1}\) simulation, the higher-density cores do not have time to form before the shock has passed through the cloud.
The mass of the cores while the red solid line shows the fit $N_{\text{core}} = 7M^{-0.6}$, giving a value of $\gamma = 1.6$ for Equation (5) in agreement with the observed value for the Orion molecular cloud.

(A color version of this figure is available in the online journal.)

**Table 4**  
Properties of the Five Most Massive Cores at the Point of Maximum Core Number, 2.5 Myr in the 5CC Simulation

| $M$ ($M_\odot$) | $r_{\text{core}}$ (pc) | $\dot{n}$ (cm$^{-3}$) | $\sigma$ (km s$^{-1}$) | $\alpha_{\text{vir}}$ | $M$ ($M_\odot$ yr$^{-1}$) |
|----------------|------------------------|----------------------|-----------------------|----------------------|-------------------------|
| 18.15          | 0.26                   | 1.16E+04             | 0.27                  | 2.31                 | 2.11E-04                |
| 6.83           | 0.20                   | 7.00E+03             | 0.17                  | 3.09                 | 1.08E-04                |
| 3.90           | 0.17                   | 7.27E+03             | 0.19                  | 4.94                 | 2.55E-05                |
| 2.85           | 0.15                   | 7.81E+03             | 0.17                  | 5.60                 | 1.37E-05                |
| 1.79           | 0.13                   | 6.80E+03             | 0.11                  | 5.71                 | 1.06E-05                |

**Table 5**  
Properties of the Five Most Massive Cores at the Point of Maximum Core Number, 1.4 Myr in the 10CC Simulation

| $M$ ($M_\odot$) | $r_{\text{core}}$ (pc) | $\dot{n}$ (cm$^{-3}$) | $\sigma$ (km s$^{-1}$) | $\alpha_{\text{vir}}$ | $M$ ($M_\odot$ yr$^{-1}$) |
|----------------|------------------------|----------------------|-----------------------|----------------------|-------------------------|
| 0.50           | 0.09                   | 4.06E+03             | 0.22                  | 24.11                | 6.18E-06                |
| 0.48           | 0.09                   | 4.51E+03             | 0.30                  | 33.17                | 4.99E-06                |
| 0.46           | 0.08                   | 4.52E+03             | 0.22                  | 23.59                | 7.12E-06                |
| 0.45           | 0.09                   | 4.40E+03             | 0.27                  | 31.80                | 5.39E-06                |
| 0.44           | 0.08                   | 4.83E+03             | 0.43                  | 58.34                | 7.72E-06                |

Cores are typically unbound with only the largest cores in simulations 3CC and 5CC obtaining an $\alpha_{\text{vir}}$ close to the threshold for gravitational binding. In fact, a more accurate calculation of this property reveals that both of those cores are bound, but the rest remain unbound. This is reflected in their mass with the bound cores reaching a mass several times larger than the next biggest candidate through runaway growth. This mass increase will also be explored in Section 4.5.3. The cores continue to grow past the time shown in the tables, but the unbound cores ultimately begin to lose mass once the shock has passed and dissipate as shown in the core number plots in Figure 10. The number of unbound cores makes it possible that only a single object in these small clouds will survive to collapse and form a massive star or super star cluster.

The core masses can be explored by looking at the cumulative mass distribution (CMD) shown in Figure 11. Here, we restrict the cores plotted to those containing a minimum of 27 cells (approximately 3 cells in each dimension) to ensure the best resolution. Due to the size of the cores formed in the 10CC case, the cores were not resolved enough to plot the CMD for this run. The CMD is derived from the core mass function, $\phi$, defined as

$$\phi \equiv \frac{dN}{dM} \propto M^{-\gamma}, \quad (5)$$

where $M$ is the core mass and $dN$ is the number of cores with masses between $M$ and $M+dM$. The cumulative mass function is then given by the integral

$$N(> M) = \int_{M}^{\infty} \frac{dN}{dM} dM \propto M^{-(\gamma-1)}. \quad (6)$$

The red solid line in Figure 11 shows a power law with equation $N_{\text{core}}(> M) = 7M^{-0.6}$, giving $\gamma = 1.6$. This value agrees with observational results from Tatamatsu (1993), who found that cores in the Orion A molecular cloud fit a value of $\gamma = 1.6 \pm 0.3$ for $M \gtrsim 50 M_\odot$ (the completeness limit of their survey). At masses closer to our own cores, Scalo (1985) found $\gamma = -1.5$ to $-1.0$ for Orion A cores with $M \approx 4 M_\odot$ and Stutzki & Guesten (1990) found $\gamma = -1.7$ for $M \approx 10 M_\odot$ for cores in the M17 SW region. In Orion B, Johnstone et al. (2001) found $\gamma = -1.5$ to $-2.0$ for $M > 1.0 M_\odot$. In general, these values are similar to the Salpeter stellar initial mass function (IMF; Salpeter 1955), although it remains unclear whether the core and ultimate stellar size are directly connected. Simulations of the collapse of a single isothermal cloud performed by Klessen et al. (1998) also found agreement with $\gamma = -1.5$ for cores formed in their fragmented gas, while a comparison of clouds fragmenting with different initial density profiles by Girichidis et al. (2011) likewise found a Salpeter consistent value of $\gamma = -1.35$ for all models. These similarities suggest that triggered core formation should take a similar form to more quiescent core creation. However, the timescale is liable to be significantly shorter, since even in the absence of turbulence, the free-fall time of the clouds is longer than their collisional interaction. This potentially produces a different IMF, as the fast-forming cores may be able to gain a higher mass before feedback effects stunt their growth.
4.5.3. Bound Core Evolution

From the point of star formation, the most interesting structures to develop will be the gravitationally bound cores. These are the objects most likely to collapse and form stars. As shown in the previous sections, despite many cores being produced in the collision, only a single bound core is formed in the 3CC and 5CC runs. Due to the collision process being short in the 10 km s\(^{-1}\) case, this run does not form any bound cores.

A bound core can potentially form in two ways. First, it can collapse directly from shocked gas to form a sufficiently dense structure that its potential energy already exceeds its kinetic. Alternatively, it can begin life as an unbound core and gather mass via accretion of the surrounding diffuse gas or through a merger with another core. The evolution of the bound cores is shown in Figure 12, plotted over the fraction of Cloud 1’s free-fall time. The black line marks the core’s actual mass while the red dashed line marks the core’s effective Jeans mass as defined by \(M_{\text{eff}} = \frac{\sigma_{\text{th}}^3}{2 \pi G \rho_{\text{acc}}}\), where \(\sigma_{\text{th}}\) and \(\rho_{\text{acc}}\) are the average thermal velocity dispersion and density of a sphere surrounding (but not including) the core with radius, \(r_{\text{acc}}\), given by the Bondi radius:

\[
r_{\text{acc}} = \frac{2GM}{\sigma_{\text{th}}^2} + r_{\text{core}},
\]

up to a maximum of 1 pc, that is, the width of the shock front (Bondi 1951). Note that since we do not include the core gas in the accretion calculation, we add the core radius to the Bondi radius to ensure a reasonable sample of gas outside the core.

Finally, the pink dashed line shows the gas supply rate, defined as half the core’s mass or its effective Jeans mass (whichever is larger) over its free-fall time, \(\frac{0.5 \ M_{\text{core}}, \ M_{\text{eff}}}{t_{\text{ff}}}\), whose axis is on the right.

What cannot be seen so easily from Figure 10 is whether this mass gain occurs through mergers or accretion.

In the 3 km s\(^{-1}\) simulation, the core growth is predominantly due to accretion. It surpasses the effective Jeans mass at \(t/t_{\text{ff}} \sim 0.55\) and grows to a mass of 700 \(M_\odot\). The same is almost true for the bound core in the 5 km s\(^{-1}\) simulation. Growth is predominantly by accretion, yet a jump can be seen between 0.6–0.7 that represents a merger scenario. It is therefore likely that cores grow by both accretion and mergers with other neighboring cores, with accretion playing the most dominant role. In the 10 km s\(^{-1}\) simulation, the core growth is insufficient to be gravitationally bound before \(t/t_{\text{ff}} = 0.3\), the time for the shock wave to propagate through Cloud 1. The accretion rate can initially explain the early core growth until \(t/t_{\text{ff}} = 0.15\), after which point the core struggles to gain mass. This may be due to the shock leaving the core region, which causes the hydrodynamic flow around the low-mass core to disrupt it.

In reality, the maximum mass of the star forming from a gas core will be limited by the radiative heating from the forming stellar object. Once the star has formed, Bondi–Hoyle accretion (as plotted by our blue dashed line in Figure 12) is expected to only be efficient up to masses of 10 \(M_\odot\). From Figure 12, the bound cores in the 3CC and 5CC simulations reach their Jeans mass at approximately 2 \(M_\odot\) and 3 \(M_\odot\), respectively. If stars are formed at this point, then 1–2 \(M_\odot\) stars will be created, allowing for 50% of the core’s gas to escape as outflows as suggested by the analytical estimates of McKee & Tan (2002) and Matzner & McKee (2000) and the simulation comparisons of Federrath & Klessen (2012). However, if the cores are prevented from collapsing (for instance, by magnetic fields or turbulence unresolved in our simulation), then the core may continue to follow the black line in Figure 12 before forming a star. In this situation, the core will only collapse to form a massive star if the ram pressure from the infalling gas can exceed that of the outward radiation pressure. Using dimensional arguments, McKee & Tan (2002) argue that the rate of gas flow during the collapse into a star should be given by \(m_* \sim m_{\text{acc}}/t_{\text{ff}}\), where \(m_*\) is the instantaneous stellar mass. Using this, we can argue that \(m_*\) should be either half the core mass or the effective Jeans mass (since gas mass below this value will not collapse), whichever is larger. This gives the rate of gas feeding the new star as \(m_* \sim (\max(0.5 \ M_{\text{core}}, \ M_{\text{eff}}) )/t_{\text{ff}}\), which we plot as the pink dashed line in Figure 12 with the axis shown on the right. If the core is able to grow to 200 \(M_\odot\) (\(m_* = 100 \ M_\odot\)), then the supply rate will be \(3 \times 10^{-4} \ M_\odot\) yr\(^{-1}\).
a value very close to the $6 \times 10^{-4} M_\odot \text{yr}^{-1}$ rate that McKee &
Tan (2002) estimate is required to form a 100 $M_\odot$ star.

5. HIGH-RESOLUTION STUDY

To assess how our results are affected by resolution, we reran
the 5 km s$^{-1}$ relative velocity collision case with a limiting
resolution of 0.03 pc, increasing the resolution from our model
in Section 4 by a factor of two. The evolution of the collision is
shown in the surface density images in Figure 13 for the same
times as for the 5CC case in the middle row of Figure 6. The
progression of the collision is very similar in both the low-
and high-resolution runs with the smaller cloud penetration
producing the characteristic arc of shocked gas which then
collapses into a dense region of cores.

The quantitative study of the gas properties is shown in
Figure 14, which shows the gas PDF (left), core number
evolution (center), and the core CMD (right). The gas PDF
is almost identical to its low-resolution counterpart in Figure 8
with the high-density gas forming a non-log-normal wing. This
suggests that the quantity of core-forming gas is the same
in the higher-resolution run, but the core number evolution
(middle panel) shows that the extra refinement does allow
a larger number of cores to be formed at the lower two
threshold densities. In the case of our lowest threshold, $\rho =
5 \times 10^{-21}$ g cm$^{-3}$, cores are formed before the collision, but
the higher-threshold cores continue forming only within the
collisional shock. The ability to follow the collapse of smaller
objects also allows cores to be formed earlier, allowing them
potentially more time to accrete within the shock front. This
added bonus, however, only has a small benefit to the higher-
mass cores which appear at about the same time in both the high-
and low-resolution runs at $t/\tau_{\text{ff}} \approx 0.6$. 1 Myr after the shock
exits Cloud 2 (the cut-off point for the core number evolution plot),
both the 5CC and 5CCHR have formed one bound core, with
this number increasing to three bound cores for 5CCHR
0.5 Myr later.

The right-hand panel of Figure 14 shows the CMD in
the higher-resolution case. The solid red line shows the fit
$N_{\text{core}}(> M) = 5M^{-0.8}$, giving $\gamma = -1.8$. This is very close
to (though slightly steeper than) the $\gamma = -1.6$ 5CC fit, which
is shown as a red dashed line. The added refinement has pulled
in the maximum mass the cores achieve to below 10 $M_\odot$, while
increasing the number of low-mass cores below $M < 1 M_\odot$.

Overall, the evolution of the higher-resolution case is ex-
tremely close to that of its low-resolution counterpart. The same
overall quantity of dense gas is formed in the shock which trans-
lates to a similar number of high-density and bound cores.

6. DISCUSSION AND CONCLUSIONS

We explored the formation and evolution of pre-stellar gas
cores in the collision of non-identical clouds with Bonner–Ebert
profiles using hydrodynamical simulations. For the majority of
our runs, the limiting resolution was 0.06 pc, with one additional
run performed at 0.03 pc. We compared the effect of collisional speed on the core formation and examined the development of bound cores formed during the impact.

In all cases, the collision between the two clouds produces a shocked disk of gas where the clouds’ surfaces meet. Due to the size difference between the two clouds, the shock front becomes oblique as the clouds merge, pressing down on the shocked disk to form a crescent structure that is commonly observed in observations of suspected cloud–cloud collision events (Ohama et al. 2010; Furukawa et al. 2009).

Without turbulence, the smaller cloud is then compressed by its own gravity and the oblique shock, creating a single core. When turbulence is added, the shock front is comprised of filaments which lie at a range of angles to the propagating wave. These form thin shell instabilities, producing ripples that ultimately fragment into multiple cores.

The number of cores produced is proportional to the relative collision speed between the clouds. A faster collision forms cores more quickly and in greater numbers. However, the subsequent growth of these cores is controlled by how long they remain in the high-density shock front. While core mergers can play a role in increasing core mass, the majority of the mass is gained via accretion. This happens most efficiently while the background density is high, that is, while the core is inside the shocked disk. If the shock moves too fast, the cores exit the disk before they have had enough time to gain sufficient mass to become bound. These two processes (core formation and core growth) dictate the ideal shock speed for core production: fast enough to allow significant core formation, but slow enough to give these cores time to accrete.

The potential of significantly star-forming gas is seen in the cloud PDFs. With an initially turbulent structure, the clouds begin with a log-normal profile at high densities. However, when core formation starts, a non-log-normal tail develops. This agrees with observational results by Kainulainen et al. (2009), who observed that GMCs possessed such a tail once they began forming stars. A similar result was also found in Orion B by Schneider et al. (2013). This evolution in the PDF is intricately linked with the production of turbulence in the clouds. As the shock front forms between the clouds, compressive turbulence modes are formed which increase the star formation efficiency and lead to the PDF tail.

The CMD for the cores fit a power law with $\gamma = -1.6$ (from Equation (5)), in good agreement with observed cores inside GMCs. This suggests that cores formed in cloud collisions may resemble those in quiescent star formation, although the increased density of the shocked disk would be expected to increase both initial core size and accretion speed. Indeed, if allowed to collapse without colliding, our clouds only form a small number of low-density ($\rho = 5 \times 10^{-21}$ g cm$^{-3}$) cores and do not produce objects close to the observed density of star-forming regions (Lada et al. 2010).

The fact that we produce substantially more massive cores in the collision than are formed through gravitational collapse alone is an indication that this process may be important for massive star formation. However, since accretion is the dominant form of core growth in our colliding clouds, the resulting stars are unlikely to exceed $10 M_\odot$. Two possible effects may change this result. The first is the size of our clouds, which are at the lower end of the observed GMC mass distribution. A collision between larger clouds or clouds with initially higher densities may result in more massive fragmentation, producing larger cores prior to accretion. The second possibility is that cores are prevented from collapse by magnetic fields or turbulence that we are not resolving at our current resolution. This would permit the cores to grow via accretion before radiation from the forming star cuts the gas flow. We will consider these effects in later work.

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