Electric field effect modulation of transition temperature, mobile carrier density and in-plane penetration depth in NdBa$_2$Cu$_3$O$_{7−\delta}$ thin films

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We explore the relationship between the critical temperature, $T_c$, the mobile areal carrier density, $n_{2D}$, and the zero temperature magnetic in-plane penetration depth, $\lambda_{ab}(0)$, in very thin underdoped NdBa$_2$Cu$_3$O$_{7−\delta}$ films near the superconductor to insulator transition using the electric field effect technique. Having established consistency with a Kosterlitz-Thouless transition we observe that $T_K(T)$ depends linearly on $n_{2D}$, the signature of a quantum superconductor to insulator transition in two dimensions with $\gamma = 1$, where $\gamma$ is the dynamic and $\nu$ the critical exponent of the in-plane correlation length.

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The electronic properties of high $T_c$ superconductors are critically determined by the density of mobile holes as illustrated by their generic phase diagram in the temperature dopant concentration plane. Understanding the physics of this phase diagram, in particular at the two $T = 0$ edges of the superconducting dome, has emerged as one of the critical questions in the field of cuprate superconductors. In the underdoped regime, where a superconductor to insulator transition occurs, there is an empirical linear relation (the so-called Uemura relation) between $T_c$ and $\lambda_{ab}^2(0)$, where $\lambda_{ab}$ is the in-plane London penetration depth. If, in the underdoped limit, a two dimensional (2D) quantum superconductor to insulator (QSI) transition occurs, such a relation between $T_c$ and $1/\lambda^2(0)$ is expected. This however necessitates the occurrence of a 3D to 2D crossover as the underdoped limit is approached with a diverging anisotropy $\gamma = \lambda_c/\lambda_{ab}$. In the case of a 3D QSI-transition, one would expect $T_c \propto \lambda_{ab}(0)^{-2z/(z+1)}$, where $z$ is the dynamic critical exponent of the transition. Recent penetration depth measurements on YBa$_2$Cu$_3$O$_{6+x}$ single crystals (where $\gamma$ apparently saturates at low doping levels) and films suggest a 3D-transition with $2z/(z+1) \approx 1$, a result different from the Uemura relation. Furthermore, an empirical relation involving the normal state conductivity and extending up to optimum doping was recently proposed by Homes et al. However, all these studies on the relationship between $T_c$ and $\lambda_{ab}(0)$ stem from samples where the doping level was modified by chemical substitution.

In this letter we use the electrostatic field effect to tune the mobile areal carrier density, $n_{2D}$, in ultrathin, strongly underdoped NdBa$_2$Cu$_3$O$_{7−\delta}$ (NBCO) films and explore the intrinsic relation between $T_c$, $n_{2D}$ and $\lambda_{ab}^2(0)$ close to the superconductor to insulator transition. The electrostatic field effect technique, which allows the carrier density in a given sample to be changed without affecting the chemical composition, thus avoiding sample to sample variations and substitution induced disorder, appears to be an ideal method to elucidate the intrinsic relationships between the key physical parameters.

In a classical oxide field effect configuration, an electric field is applied across a gate dielectric in a heterostructure made of an oxide channel and a dielectric layer. The density of carriers is modified at the interface between the oxide channel and the dielectric, changing the electronic properties of the oxide channel. This technique allows us to induce in thin oxide superconducting films rather large $T_c$ modulations. In the 3-4 unit cell thick films used in this study, $T_c$ modulations of more than 10 K have been achieved, corresponding to induced charge densities of the order of $0.7 \cdot 10^{14}$ charges/cm$^2$.

The field effect device used in this study, described in Ref. [10], is based on a SrTiO$_3$ (STO) single crystal gate dielectric, the substrate itself. Due to its large low temperature dielectric constant, $\varepsilon$, and large achievable polarizations, STO is a particularly interesting gate insulator. Field effect devices using a STO thin film gate insulator have thus been studied extensively. Here, thin 100 $\mu$m thick, or thinned 500 $\mu$m commercial substrates have been used. A sketch of the thinned device is shown in the upper inset of Fig. 1. The superconducting NBCO thin films are first grown by off-axis magnetron sputtering onto (001) (bare or etched) STO substrates heated to about 730°C. During cooling, a typical O$_2$ pressure of 670 Torr is used to obtain optimally doped films. To control the initial doping level of the films, the oxygen cooling pressure is modified and lowered down to 5 mTorr for the most underdoped films. Gold is sputtered in-situ at room temperature to improve the contact resistances and the whole structure is protected by an amorphous NBCO layer also deposited in-situ. X-ray diffraction allowed us to determine precisely the film thickness down to three unit cell thick films. After deposition, the sam-
samples are photolithographically patterned using ion milling and a gold electrode is deposited on the backside of the samples, facing the central part of the superconducting path. The measured path is 600 (length) × 500 (width) µm². The patterning process does not affect Tc. All the thin films presented here are 3-4 unit cell thick.

Fig 1 shows resistance versus temperature for sample 1 in the tail of the transitions, for different voltages applied across the gate dielectric: 0, −20, −50, −100 and −200 V. Negative voltages correspond to a negative potential applied to the gate and a positive one to the superconducting path, resulting in hole doping of the oxide channel and, as expected, in a “shift” to higher temperatures of the resistive transition. Resistance measurements are performed using a standard four point technique while a voltage, Vg, is applied to the gate. During measurements, gate leakage currents were kept below a few nA, while the current used for resistance measurements was typically between 1 and 10 µA. The lower inset of Fig 1 shows resistance versus temperature for sample 5 and for gate voltages of 400, 200, 100, 50, 20, 10, 0, −5, −20, −50, −100, and −200 V. At 4.2 K, a large increase in resistance is observed while applying positive gate voltages, effectively reducing the hole concentration.

To estimate Tc, we explore the consistency of our resistivity data with the expected behavior for a Kosterlitz-Thouless (KT) transition, namely ρ = ρ0 exp(−bt−1/2), where t = T/Tc − 1 and ρ0 and b are material dependent but temperature independent parameters. Accordingly, consistency with the KT-scenario is established when the plot (∂ ln R/∂T)−2/3 vs. t exhibits, near t = 0, linear behavior and Tc = TKT is determined by the condition (∂ ln R/∂T)−2/3 = 0 at TKT.

Fig 2: (∂ ln R/∂T)−2/3 vs. T for samples 1 and 5 at various gate voltages. The solid lines indicate the consistency with the linear KT relationship. Tc = TKT is determined by the condition (∂ ln R/∂T)−2/3 = 0 at TKT.
reveals the intrinsic linear relationship

\[ \Delta T_{KT} = 1.3 \times 10^{-13} \Delta n_{2D}, \]  

(1)

where \( \Delta T_{KT} = T_{KT}(V) - T_{KT}(0) \) and \( \Delta n_{2D} \) is expressed in cm\(^{-2}\). This is a novel and central result of our paper.

Together with the quantum counterpart of the Nelson-Kosterlitz relation, \( T_{KT} \propto \lambda_{ab}^{-2}(T_{KT}) \), it implies that \( T_{KT} \), \( \lambda_{ab}(0) \) and \( n_{2D} \) are universally related by

\[ T_{KT} \propto n_{2D} \propto \frac{1}{\lambda_{ab}^2(0)}, \]  

(2)

with non-universal factors of proportionality. This relationship also confirms the theoretical predictions for a 2D-QSI transition. Indeed, the scaling theory of quantum critical phenomena [2, 10] predicts that close to a QSI transition \( T_c \) scales as \( n_{2D}^{-\nu} \), where \( \nu \) is the dynamic critical exponent of the zero temperature in-plane correlation length, \( \xi_{ab} \propto n_{2D}^{-\nu} \). Thus, Eq. (2) reveals that \( \nu \approx 1 \), the signature of a QSI transition in 2D [14, 15]. Since close to a QSI transition \( \lambda_{ab}(0) \) scales as \( 1/\lambda_{ab}(0) \propto n_{2D}^{(D+z-2)} \) \( (D \) is the system dimensionality) [2, 10], it follows that \( \Delta T_{KT} \propto \Delta n_{2D} \) does not only uncover a 2D-QSI transition with \( \pi \approx 1 \), but also implies that \( T_{KT} \), \( \lambda_{ab}(0) \) and \( n_{2D} \) are universally related by Eq. (2). However, this relationship differs drastically from \( T_c \propto 1/\lambda_{a,b,c}(0) \), derived from penetration depth measurements on YBa\(_2\)Cu\(_3\)O\(_{6+x}\) single crystals [3, 4] and films [5], where \( T_c \) was reduced by chemical substitution.

To substantiate our main result further, we explore the temperature, electric and magnetic field dependence of the resistive transition, extracting the activation energy, \( U \), for vortex motion in the liquid vortex phase. In the vortex 2D-limit the resistance in a field is activated with activation energy proportional to \( -\ln(H) \). The measurements have been performed with the magnetic field applied perpendicular to the \( ab \)-plane, ramping the temperature slowly and measuring the sample resistance at a given magnetic and electric field. Inset of Fig. 4 shows Arrhenius plots of the resistivity, \( \rho \), as a function of \( 1/T \) for sample 2 and for three different electric fields at \( 0.1T \). The zero temperature activation energy \( U_0 \) at a given applied electrical field is obtained from the slope of the Arrhenius plot. The solid line is Eq. (1).

FIG. 3: (a) Right scale, \( T_{KT} \) versus gate voltage \( V \). The solid lines are \( T_{KT}(V) \propto T_{KT}(0) + a|V|^{1/2} \) with \( a = 0.54 \), 0.62, 0.32, 0.34 for samples 1, 2, 5 and 6. Left scale, \( dQ/dV \) versus \( V \) for a 100\( \mu \)m thick STO measured at 4.2 K using an electrometer (open circles), \( C(V) \) measured using an LCR-meter (open squares). (b) \( \Delta T_{KT} \) vs. \( \Delta n_{2D} \) for all the samples. The solid line is Eq. (1).

FIG. 4: \( U_0/k_B \) vs. \( H \) for different applied voltages for sample 1. A linear relation between \( U_0 \) and \( \log(H) \) is observed with a slope which depends on the applied electric field. Inset: \( \log(U) \) as a function of \( 1/T \) for sample 2 and for three different electric fields at 0.1T. The zero temperature activation energy \( U_0 \) at a given applied electrical field is obtained from the slope of the Arrhenius plot.
characteristic 2D logarithmic field dependence $U_0(H) = -\alpha \ln(H) + \beta$, in agreement with previous measurements on thin films, superlattices, and the highly anisotropic kappa-(BEDT-TTF)$_2$Cu(NCS)$_2$. Note that in 3D $U \propto H^{-1/2}$ is expected [26]. Furthermore we find that $T_c = T_{KT}$ is proportional to $U_0(H)/k_B$ for every value of the magnetic field. Since $U$ is proportional to $1/\lambda^2_{ab}$ in $D = 2$ (and $D = 3$) [22, 24], this proportionality is also consistent with our main result $T_c \propto n_{2D} \propto 1/\lambda^2_{ab}(0)$.

In summary, we explored the relationships between $T_c$, the mobile areal carrier density, $n_{2D}$, and the zero temperature in-plane penetration depth, $\lambda_{ab}(0)$, for very thin underdoped NBCO films near the superconductor to insulator transition by means of the electric field effect technique. Together with the observed behavior of the resistive transition we established remarkable consistency between 2D critical behavior and a quantum superconductor to insulator transition, characterized by a linear relationship between $T_c$, $n_{2D}$ and $1/\lambda^2_{ab}(0)$. This result also implies that isotope or pressure effects on $T_c$, $n_{2D}$ and $\lambda_{ab}(0)$ are related accordingly.

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[27] $dQ$ is obtained for a $dV$ of 1V. Also $C(V)$ was measured with voltage modulation amplitudes between 0.1 and 1V.
[28] Except for sample 6 where $\Delta T_{KT} = T_{KT}(V) - T_{KT}(\pm 50V)$. 
