PCFGs, Topic Models, Adaptor Grammars and Learning Topical Collocations and the Structure of Proper Names

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Abstract
This paper establishes a connection between two apparently very different kinds of probabilistic models. Latent Dirichlet Allocation (LDA) models are used as “topic models” to produce a low-dimensional representation of documents, while Probabilistic Context-Free Grammars (PCFGs) define distributions over trees. The paper begins by showing that LDA topic models can be viewed as a special kind of PCFG, so Bayesian inference for PCFGs can be used to infer Topic Models as well. Adaptor Grammars (AGs) are a hierarchical, non-parametric Bayesian extension of PCFGs. Exploiting the close relationship between LDA and PCFGs just described, we propose two novel probabilistic models that combine insights from LDA and AG models. The first replaces the unigram component of LDA topic models with multi-word sequences or collocations generated by an AG. The second extension builds on the first one to learn aspects of the internal structure of proper names.

1 Introduction
Over the last few years there has been considerable interest in Bayesian inference for complex hierarchical models both in machine learning and in computational linguistics. This paper establishes a theoretical connection between two very different kinds of probabilistic models: Probabilistic Context-Free Grammars (PCFGs) and a class of models known as Latent Dirichlet Allocation (Blei et al., 2003; Griffiths and Steyvers, 2004) models that have been used for a variety of tasks in machine learning. Specifically, we show that an LDA model can be expressed as a certain kind of PCFG, so Bayesian inference for PCFGs can be used to learn LDA topic models as well. The importance of this observation is primarily theoretical, as current Bayesian inference algorithms for PCFGs are less efficient than those for LDA inference. However, once this link is established it suggests a variety of extensions to the LDA topic models, two of which we explore in this paper. The first involves extending the LDA topic model so that it generates collocations (sequences of words) rather than individual words. The second applies this idea to the problem of automatically learning internal structure of proper names (NPs), which is useful for definite NP coreference models and other applications.

The rest of this paper is structured as follows. The next section reviews Latent Dirichlet Allocation (LDA) topic models, and the following section reviews Probabilistic Context-Free Grammars (PCFGs). Section 4 shows how an LDA topic model can be expressed as a PCFG, which provides the fundamental connection between LDA and PCFGs that we exploit in the rest of the paper, and shows how it can be used to define a “sticky topic” version of LDA. The following section reviews Adaptor Grammars (AGs), a non-parametric extension of PCFGs introduced by Johnson et al. (2007b). Section 6 exploits the connection between LDA and PCFGs to propose an AG-based topic model that extends LDA by defining distributions over collocations rather than individual words, and section 7 applies this extension to the problem of finding the structure of proper names.

2 Latent Dirichlet Allocation Models
Latent Dirichlet Allocation (LDA) was introduced as an explicit probabilistic counterpart to Latent Semantic Indexing (LSI) (Blei et al., 2003). Like LSI, LDA is intended to produce a low-dimensional characterisation or summary of a doc-
Figure 1: A graphical model “plate” representation of an LDA topic model. Here \( \ell \) is the number of topics, \( m \) is the number of documents and \( n \) is the number of words per document.

An LDA model is an explicit generative probabilistic model of a collection of documents. We describe the “smoothed” LDA model here (see page 1006 of Blei et al. (2003)) as it corresponds precisely to the Bayesian PCFGs described in section 4. It generates a collection of documents by first generating multinomials \( \phi_i \) over the vocabulary \( V \) for each topic \( i \in 1, \ldots, \ell \), where \( \ell \) is the number of topics and \( \phi_{i,w} \) is the probability of generating word \( w \) in topic \( i \). Then it generates each document \( D_j, j = 1, \ldots, m \) in turn by first generating a multinomial \( \theta_j \) over topics, where \( \theta_{j,i} \) is the probability of topic \( i \) appearing in document \( j \). (\( \theta_j \) serves as the low-dimensional representation of document \( D_j \)). Finally it generates each of the \( n \) words of document \( D_j \) by first selecting a topic \( z \) for the word according to \( \theta_j \), and then drawing a word from \( \phi_z \). Dirichlet priors with parameters \( \beta \) and \( \alpha \) respectively are placed on the \( \phi_i \) and the \( \theta_j \) in order to avoid the zeros that can arise from maximum likelihood estimation (i.e., sparse data problems).

The LDA generative model can be compactly expressed as follows, where “\( \sim \)” should be read as “is distributed according to”.

\[
\begin{align*}
\phi_i & \sim \text{Dir}(\beta) & i = 1, \ldots, \ell \\
\theta_j & \sim \text{Dir}(\alpha) & j = 1, \ldots, m \\
z_{j,k} & \sim \theta_j & j = 1, \ldots, m; k = 1, \ldots, n \\
w_{j,k} & \sim \phi_{z,j,k} & j = 1, \ldots, m; k = 1, \ldots, n
\end{align*}
\]

In inference, the parameters \( \alpha \) and \( \beta \) of the Dirichlet priors are either fixed (i.e., chosen by the model designer), or else themselves inferred, e.g., by Bayesian inference. (The adaptor grammar software we used in the experiments described below automatically does this kind of hyper-parameter inference).

The inference task is to find the topic probability vector \( \theta_j \) of each document \( D_j \) given the words \( w_{j,k} \) of the documents; in general this also requires inferring the topic to word distributions \( \phi \) and the topic assigned to each word \( z_{j,k} \). Blei et al. (2003) describe a Variational Bayes inference algorithm for LDA models based on a mean-field approximation, while Griffiths and Steyvers (2004) describe an Markov Chain Monte Carlo inference algorithm based on Gibbs sampling; both are quite effective in practice.

3 Probabilistic Context-Free Grammars

Context-Free Grammars are a simple model of hierarchical structure often used to describe natural language syntax. A Context-Free Grammar (CFG) is a quadruple \( (N, W, R, S) \) where \( N \) and \( W \) are disjoint finite sets of nonterminal and terminal symbols respectively, \( R \) is a finite set of productions or rules of the form \( A \rightarrow \beta \) where \( A \in N \) and \( \beta \in (N \cup W)^* \), and \( S \in N \) is the start symbol.

In what follows, it will be useful to interpret a CFG as generating sets of finite, labelled, ordered trees \( T_A \) for each \( X \in N \cup W \). Informally, \( T_X \) consists of all trees \( t \) rooted in \( X \) where for each local tree \( (B, \beta) \) in \( t \) (i.e., where \( B \) is a parent’s label and \( \beta \) is the sequence of labels of its immediate children) there is a rule \( B \rightarrow \beta \in R \).

Formally, the sets \( T_X \) are the smallest sets of trees that satisfy the following equations.

If \( X \in W \) (i.e., if \( X \) is a terminal) then \( T_X = \{X\} \), i.e., \( T_X \) consists of a single tree, which in turn only consists of a single node labelled \( X \).

If \( X \in N \) (i.e., if \( X \) is a nonterminal) then

\[
T_X = \bigcup_{X \rightarrow B_1 \ldots B_n \in R_X} \text{Tree}_X(T_{B_1}, \ldots, T_{B_n})
\]

where \( R_A = \{A \rightarrow \beta: A \rightarrow \beta \in R\} \) for each \( A \in N \), and

\[
\text{Tree}_X(T_{B_1}, \ldots, T_{B_n}) = \left\{ X \rightarrow t_1 \ldots t_n : t_i \in T_{B_i}, \quad i = 1, \ldots, n \right\}
\]

That is, \( \text{Tree}_X(T_{B_1}, \ldots, T_{B_n}) \) consists of the set of trees with whose root node is labelled \( X \) and whose \( i \)th child is a member of \( T_{B_i} \).
The set of trees generated by the CFG is \( T_S \), where \( S \) is the start symbol, and the set of strings generated by the CFG is the set of yields (i.e., terminal strings) of the trees in \( T_S \).

A Probabilistic Context-Free Grammar (PCFG) is a pair consisting of a CFG and set of multinomial probability vectors \( \theta_X \) indexed by nonterminals \( X \in N \), where \( \theta_X \) is a distribution over the rules \( R_X \) (i.e., the rules expanding \( X \)). Informally, \( \theta_{X \rightarrow \beta} \) is the probability of \( X \) expanding to \( \beta \) using the rule \( X \rightarrow \beta \in R_X \). More formally, a PCFG associates each \( X \in N \cup W \) with a distribution \( G_X \) over the trees \( T_X \) as follows.

If \( X \in W \) (i.e., if \( X \) is a terminal) then \( G_X \) is the distribution that puts probability 1 on the single-node tree labelled \( X \).

If \( X \in N \) (i.e., if \( X \) is a nonterminal) then:

\[
G_X = \sum_{X \rightarrow B_1...B_n \in R_X} \theta_{X \rightarrow B_1...B_n} \text{TD}_X(G_{B_1}, ..., G_{B_n})
\]

where:

\[
\text{TD}_A(G_1, ..., G_n) \left( \begin{array}{c} X \\ t_1 \ldots t_n \end{array} \right) = \prod_{i=1}^{n} G_i(t_i).
\]

That is, \( \text{TD}_A(G_1, ..., G_n) \) is a distribution over \( T_A \) where each subtree \( t_i \) is generated independently from \( G_i \). These equations have solutions (i.e., the PCFG is said to be “consistent”) when the rule probabilities \( \theta_A \) obey certain conditions; see e.g., Wetherell (1980) for details.

The PCFG generates the distribution over trees \( G_S \), where \( S \) is the start symbol. The distribution over the strings it generates is obtained by marginalising over the trees.

In a Bayesian PCFG one puts Dirichlet priors \( \text{Dir}(\alpha_X) \) on each of the multinomial rule probability vectors \( \theta_X \) for each nonterminal \( X \in N \). This means that there is one Dirichlet parameter \( \alpha_{X \rightarrow \beta} \) for each rule \( X \rightarrow \beta \in R \) in the CFG.

In the “unsupervised” inference problem for a PCFG one is given a CFG, parameters \( \alpha_X \) for the Dirichlet priors over the rule probabilities, and a corpus of strings. The task is to infer the corresponding posterior distribution over rule probabilities \( \theta_X \). Recently Bayesian inference algorithms for PCFGs have been described. Kurihara and Sato (2006) describe a Variational Bayes algorithm for inferring PCFGs using a mean-field approximation, while Johnson et al. (2007a) describe a Markov Chain Monte Carlo algorithm based on Gibbs sampling.

4 LDA topic models as PCFGs

This section explains how to construct a PCFG that generates the same distribution over a collection of documents as an LDA model, and where Bayesian inference for the PCFG’s rule probabilities yields the corresponding distributions as Bayesian inference of the corresponding LDA models. (There are several different ways of encoding LDA models as PCFGs; the one presented here is not the most succinct — it is possible to collapse the Doc and Doc’ nonterminals — but it has the advantage that the LDA distributions map straight-forwardly onto PCFG nonterminals).

The terminals \( W \) of the CFG consist of the vocabulary \( V \) of the LDA model plus a set of special “document identifier” terminals “\( \cdot \)” for each document \( j \in 1, \ldots, m \), where \( m \) is the number of documents. In the PCFG encoding strings from document \( j \) are prefixed with “\( \cdot \)”; this indicates to the grammar which document the string comes from. The nonterminals consist of the start symbol Sentence, Doc\( j \) and Doc’\( j \) for each \( j \in 1, \ldots, m \), and Topic\( i \) for each \( i \in 1, \ldots, \ell \), where \( \ell \) is the number of topics in the LDA model.

The rules of the CFG are all instances of the following schemata:

\[
\begin{align*}
\text{Sentence} & \rightarrow \text{Doc}_j, \quad j \in 1, \ldots, m \\
\text{Doc}_j & \rightarrow \cdot j, \quad j \in 1, \ldots, m \\
\text{Doc}_j & \rightarrow \text{Doc}_j \text{Doc}_j, \quad j \in 1, \ldots, m \\
\text{Doc}_j & \rightarrow \text{Topic}_i, \quad i \in 1, \ldots, \ell; j \in 1, \ldots, m \\
\text{Topic}_i & \rightarrow w, \quad i \in 1, \ldots, \ell; w \in V
\end{align*}
\]

Figure 2 depicts a tree generated by such a CFG. The relationship between the LDA model and the PCFG can be understood by studying the trees generated by the CFG. In these trees the left-branching spine of nodes labelled Doc\( j \) propagate the document identifier throughout the whole tree. The nodes labelled Topic\( i \) indicate the topics assigned to particular words, and the local trees expanding Doc\( j \) to Topic\( i \) (one per word in the document) indicate the distribution of topics in the document.

The corresponding Bayesian PCFG associates probabilities with each of the rules in the CFG. The probabilities \( \theta_{\text{Topic}_i} \) associated with the rules expanding the Topic\( i \) nonterminals indicate how words are distributed across topics; the \( \theta_{\text{Topic}_i} \) probabilities correspond exactly to the \( \phi_i \) probabilities of the LDA model. The probabilities
A sample parse generated by a “sticky topic”
CFG is shown in Figure 3. The probabilities of the rules Doc_{j,i} \rightarrow Doc_{j,i'} \ Topic_i in this PCFG encode the probability of shifting from topic i to topic i' (this PCFG can be viewed as generating the string from right to left).

We can use non-uniform sparse Dirichlet priors on the probabilities of these rules to encourage “topic stickiness”. Specifically, by setting the Dirichlet parameters for the “topic shift” rules Doc_{j,i'} \rightarrow Doc_{j,i} \ Topic_i where i' \neq i much lower than the parameters for the “topic preservation” rules Doc_{j,i} \rightarrow Doc_{j,i} \ Topic_i, Bayesian inference will be biased to find distributions in which adjacent words will tend to have the same topic.

5 Adaptor Grammars

Non-parametric Bayesian inference, where the inference task involves learning not just the values of a finite vector of parameters but which parameters are relevant, has been the focus of intense research in machine learning recently. In the topic-modelling community this has lead to work on Dirichlet Processes and Chinese Restaurant Processes, which can be used to estimate the number of topics as well as their distribution across documents (Teh et al., 2006).

There are two obvious non-parametric extensions to PCFGs. In the first we regard the set of nonterminals $N$ as potentially unbounded, and try to learn the set of nonterminals required to describe the training corpus. This approach goes under the name of the “infinite HMM” or “infinite PCFG” (Beal et al., 2002; Liang et al., 2007; Liang et al., 2009). Informally, we are given a set of “basic categories”, say NP, VP, etc., and a set of rules that use these basic categories, say $S \rightarrow NP \ VP$. The inference task is to learn a set of refined categories and rules (e.g., $S_7 \rightarrow NP_2 \ VP_5$) as well as their probabilities; this approach can therefore be viewed as a Bayesian version of the “split-merge” approach to grammar induction (Petrov and Klein, 2007).

In the second approach, which we adopt here, we regard the set of rules $R$ as potentially unbounded, and try to learn the rules required to describe a training corpus as well as their probabilities. Adaptor grammars are an example of this approach (Johnson et al., 2007b), where entire subtrees generated by a “base grammar” can be viewed as distinct rules (in that we learn a separate probability for each subtree). The inference task is non-parametric if there are an unbounded number of such subtrees.

We review the adaptor grammar generative process below; for an informal introduction see Johnson (2008) and for details of the adaptor grammar inference procedure see Johnson and Goldwater (2009).

An adaptor grammar $(N, W, R, S, \theta, A, C)$ consists of a PCFG $(N, W, R, S, \theta)$ in which a subset $A \subseteq N$ of the nonterminals are adapted, and where each adapted nonterminal $X \in A$ has an associated adaptor $C_X$. An adaptor $C_X$ for $X$ is a function that maps a distribution over trees $T_X$ to a distribution over distributions over $T_X$ (we give examples of adaptors below).

Just as for a PCFG, an adaptor grammar defines distributions $G_X$ over trees $T_X$ for each $X \in N \cup W$. If $X \in W$ or $X \notin A$ then $G_X$ is defined just as for a PCFG above, i.e., using (1). However, if $X \in A$ then $G_X$ is defined in terms of an additional distribution $H_X$ as follows:

$$G_X \sim C_X(H_X)$$

$$H_X = \sum_{X \rightarrow Y_1 \ldots Y_m} \theta_{X \rightarrow Y_1 \ldots Y_m} TD_X(G_{Y_1}, \ldots, G_{Y_m})$$

That is, the distribution $G_X$ associated with an adapted nonterminal $X \in A$ is a sample from adapting (i.e., applying $C_X$ to) its “ordinary” PCFG distribution $H_X$. In general adaptors are chosen for the specific properties they have. For example, with the adaptors used here $G_X$ typically concentrates mass on a smaller subset of the trees $T_X$ than $H_X$ does.

Just as with the PCFG, an adaptor grammar generates the distribution over trees $G_S$, where $S \in N$.
is the start symbol. However, while $G_S$ in a PCFG is a fixed distribution (given the rule probabilities $\theta$), in an adaptor grammar the distribution $G_S$ is itself a random variable (because each $G_X$ for $X \in A$ is random), i.e., an adaptor grammar generates a distribution over distributions over trees $T_S$. However, the posterior joint distribution $\Pr(t)$ of a sequence $t = (t_1, \ldots, t_n)$ of trees in $T_S$ is well-defined:

$$\Pr(t) = \int G_S(t_1) \ldots G_S(t_n) \, dG$$

where the integral is over all of the random distributions $G_X, X \in A$. The adaptors we use in this paper are Dirichlet Processes or two-parameter Poisson-Dirichlet Processes, for which it is possible to compute this integral. One way to do this uses the predictive distributions:

$$\Pr(t_{n+1} \mid t, H_X) \propto \int G_X(t_1) \ldots G_X(t_{n+1}) C_X(G_X \mid H_X) \, dG_X$$

where $t = (t_1, \ldots, t_n)$ and each $t_i \in T_X$. The predictive distribution for the Dirichlet Process is the (labeled) \textit{Chinese Restaurant Process} (CRP), and the predictive distribution for the two-parameter Poisson-Dirichlet process is the (labeled) \textit{Pitman-Yor Process} (PYP).

In the context of adaptor grammars, the CRP is:

$$\text{CRP}(t \mid t, \alpha_X, H_X) \propto n_t(t) + \alpha_X H_X(t)$$

where $n_t(t)$ is the number of times $t$ appears in $t$ and $\alpha_X > 0$ is a user-settatable “concentration parameter”. In order to generate the next tree $t_{n+1}$ a CRP either reuses a tree $t$ with probability proportional to number of times $t$ has been previously generated, or else it “backs off” to the “base distribution” $H_X$ and generates a fresh tree $t$ with probability proportional to $\alpha_X H_X(t)$.

The PYP is a generalization of the CRP:

$$\text{PYP}(t \mid t, a_X, b_X, H_X) \propto \max(0, n_t(t) - m_t a_X) + (m_X + b_X) H_X(t)$$

Here $a_X \in [0, 1]$ and $b_X > 0$ are user-settatable parameters, and $m_t$ is the number of times the PYP has generated $t$ in $t$ from the base distribution $H_X$, and $m = \sum_{t \in T_X} m_t$ is the number of times any tree has been generated from $H_X$. In the Chinese Restaurant metaphor, $m_t$ is the number of tables labeled with $t$, and $m$ is the number of occupied tables. If $a_X = 0$ then the PYP is equivalent to a CRP with $\alpha_X = b_X$, while if $a_X = 1$ then the PYP generates samples from $H_X$.

Informally, the CRP has a strong preference to regenerate trees that have been generated frequently before, leading to a “rich-get-richer” dynamics. The PYP can mitigate this somewhat by reducing the effective count of previously generated trees and redistributing that probability mass to new trees generated from $H_X$. As Goldwater et al. (2006) explain, Bayesian inference for $H_X$ given samples from $G_X$ is effectively performed from types if $a_X = 0$ and from tokens if $a_X = 1$, so varying $a_X$ smoothly interpolates between type-based and token-based inference.

Adaptor grammars have previously been used primarily to study grammatical inference in the context of language acquisition. The \textit{word segmentation task} involves segmenting a corpus of unsegmented phonemic utterance representations into words (Elman, 1990; Bernstein-Ratner, 1987). For example, the phoneme string corresponding to “you want to see the book” (with its correct segmentation indicated) is as follows:

```
y u w a n t u s i D 6 b U k
```

We can represent any possible segmentation of any possible sentence as a tree generated by the following \textit{unigram adaptor grammar}.

```
Sentence → Word
Sentence → Word Sentence
Word → Phonemes
Phonemes → Phoneme
Phonemes → Phoneme Phonemes
```

The trees generated by this adaptor grammar are the same as the trees generated by the CFG rules. For example, the following skeletal parse in which all but the Word nonterminals are suppressed (the others are deterministically inferrable) shows the parse that corresponds to the correct segmentation of the string above.

```
(Word y u) (Word w a n t) (Word t u)
(Word s i) (Word d 6) (Word b u k)
```

Because the Word nonterminal is \textit{adapted} (indicated here by underlining) the adaptor grammar learns the probability of the entire Word subtrees (e.g., the probability that $b$ $u$ $k$ is a Word); see Johnson (2008) for further details.
6 Topic models with collocations

Here we combine ideas from the unigram word segmentation adaptor grammar above and the PCFG encoding of LDA topic models to present a novel topic model that learns topical collocations. (For a non-grammar-based approach to this problem see Wang et al. (2007)). Specifically, we take the PCFG encoding of the LDA topic model described above, but modify it so that the Topic nodes generate sequences of words rather than single words. Then we adapt each of the Topic nonterminals, which means that we learn the probability of each of the sequences of words it can expand to.

\[
\begin{align*}
\text{Sentence} & \rightarrow \text{Doc}_j & j \in 1, \ldots, m \\
\text{Doc}_j & \rightarrow s_j & j \in 1, \ldots, m \\
\text{Doc}_j \rightarrow \text{Doc}_j \text{ Topic}_i & i \in 1, \ldots, \ell; j \in 1, \ldots, m \\
\text{Topic}_i \rightarrow \text{Words} & i \in 1, \ldots, \ell \\
\text{Words} & \rightarrow \text{Word} \\
\text{Words} \rightarrow \text{Words Word} \\
\text{Word} \rightarrow w & w \in V
\end{align*}
\]

In order to demonstrate that this model works, we implemented this using the publically-available adaptor grammar inference software,\(^1\) and ran it on the NIPS corpus (composed of published NIPS abstracts), which has previously been used for studying collocation-based topic models (Griffiths et al., 2007). Because there is no generally accepted evaluation for collocation-finding, we merely present some of the sample analyses found by our adaptor grammar. We ran our adaptor grammar with \(\ell = 20\) topics (i.e., 20 distinct Topic nonterminals). Adaptor grammar inference on this corpus is actually relatively efficient because the corpus provided by Griffiths et al. (2007) is already segmented by punctuation, so the terminal strings are generally rather short. Rather than set the Dirichlet parameters by hand, we placed vague priors on them and estimated them as described in Johnson and Goldwater (2009).

The following are some examples of collocations found by our adaptor grammar:

\[
\begin{align*}
\text{Topic}_0 & \rightarrow \text{cost function} \\
\text{Topic}_0 & \rightarrow \text{fixed point} \\
\text{Topic}_0 & \rightarrow \text{gradient descent} \\
\text{Topic}_0 & \rightarrow \text{learning rates} \\
\text{Topic}_1 & \rightarrow \text{associative memory} \\
\text{Topic}_1 & \rightarrow \text{hamming distance} \\
\text{Topic}_1 & \rightarrow \text{randomly chosen} \\
\text{Topic}_1 & \rightarrow \text{standard deviation} \\
\text{Topic}_3 & \rightarrow \text{action potentials} \\
\text{Topic}_3 & \rightarrow \text{membrane potential} \\
\text{Topic}_3 & \rightarrow \text{primary visual cortex} \\
\text{Topic}_3 & \rightarrow \text{visual system} \\
\text{Topic}_{10} & \rightarrow \text{nervous system} \\
\text{Topic}_{10} & \rightarrow \text{action potential} \\
\text{Topic}_{10} & \rightarrow \text{ocular dominance} \\
\text{Topic}_{10} & \rightarrow \text{visual field}
\end{align*}
\]

The following are skeletal sample parses, where we have elided all but the adapted nonterminals (i.e., all we show are the Topic nonterminals, since the other structure can be inferred deterministically). Note that because Griffiths et al. (2007) segmented the NIPS abstracts at punctuation symbols, the training corpus contains more than one string from each abstract.

\[
\begin{align*}
\text{Topic}_5 \rightarrow \text{polynomial size} & \\
\text{Topic}_{15} \rightarrow \text{threshold circuits} & \\
\text{Topic}_{11} \rightarrow \text{studied} & \\
\text{Topic}_{19} \rightarrow \text{pattern recognition algorithms} & \\
\text{Topic}_2 \rightarrow \text{feedforward neural network} & \\
\text{Topic}_1 \rightarrow \text{implementation} & \\
\text{Topic}_{11} \rightarrow \text{single} & \\
\text{Topic}_{10} \rightarrow \text{ocular dominance stripe} & \\
\text{Topic}_{12} \rightarrow \text{low} & \text{(Topic}_3 \rightarrow \text{ocularity)} \\
\text{Topic}_{12} \rightarrow \text{drift rate} & \\
\end{align*}
\]

7 Finding the structure of proper names

Grammars offer structural and positional sensitivity that is not exploited in the basic LDA topic models. Here we explore the potential for using Bayesian inference for learning linear ordering constraints that hold between elements within proper names.

The Penn WSJ treebank is a widely used resource within computational linguistics (Marcus et al., 1993), but one of its weaknesses is that it does not indicate any structure internal to base noun phrases (i.e., it presents “flat” analyses of the pre-head NP elements). For many applications it would be extremely useful to have a more elaborated analysis of this kind of NP structure. For example, in an NP coreference application, if we could determine that Bill and Hillary are both first

\(^1\)http://web.science.mq.edu.au/˜mjohnson/Software.htm
names then we could infer that Bill Clinton and Hillary Clinton are likely to refer to distinct individuals. On the other hand, because Mr in Mr Clinton is not a first name, it is possible that Mr Clinton and Bill Clinton refer to the same individual (Elsner et al., 2009).

Here we present an adaptor grammar based on the insights of the PCFG encoding of LDA topic models that learns some of the structure of proper names. The key idea is that elements in proper names typically appear in a fixed order; we expect honorifics to appear before first names, which appear before middle names, which in turn appear before surnames, etc. Similarly, many company names end in fixed phrases such as Inc. Here we think of first names as a kind of topic, albeit one with a restricted positional location. One of the challenges is that some of these structural elements can be filled by multiword expressions; e.g., de Groot can be a surname. We deal with this by permitting multi-word collocations to fill the corresponding positions, and use the adaptor grammar machinery to learn these collocations.

Inspired by the grammar presented in Elsner et al. (2009), our adaptor grammar is as follows, where adapted nonterminals are indicated by underlining as before.

\[
\begin{align*}
\text{NP} & \rightarrow (A0) (A1) \ldots (A6) \\
\text{NP} & \rightarrow (B0) (B1) \ldots (B6) \\
\text{NP} & \rightarrow \text{Unordered}^+ \\
A0 & \rightarrow \text{Word}^+ \\
\quad \ldots \\
A6 & \rightarrow \text{Word}^+ \\
B0 & \rightarrow \text{Word}^+ \\
\quad \ldots \\
B6 & \rightarrow \text{Word}^+ \\
\text{Unordered} & \rightarrow \text{Word}^+
\end{align*}
\]

In this grammar parentheses indicate optional-ity, and the Kleene plus indicates iteration (these were manually expanded into ordinary CFG rules in our experiments). The grammar provides three different expansions for proper names. The first expansion says that a proper name can consist of some subset of the six different collocation classes A0 through A6 in that order, while the second expansion says that a proper name can consist of some subset of the collocation classes B0 through B6, again in that order. Finally, the third expansion says that a proper name can consist of an arbitrary sequence of “unordered” collocations (this is intended as a “catch-all” expansion to provide analyses for proper names that don’t fit either of the first two expansions).

We extracted all of the proper names (i.e., phrases of category NNP and NNPS) in the Penn WSJ treebank and used them as the training corpora for the adaptor grammar just described. The adaptor grammar inference procedure found skeletal sample parses such as the following:

- (A0 barrett) (A3 smith)
- (A0 albert) (A2 j.) (A3 smith) (A4 jr.)
- (A0 robert) (A2 b.) (A3 van dover)
- (B0 aim) (B1 prime rate) (B2 plus) (B5 fund) (B6 inc.)
- (B0 balfour) (B1 maclaine) (B5 international) (B6 ltd.)
- (B0 american express) (B1 information services) (B6 co)
- (U abc) (U sports)
- (U sports illustrated)
- (U sports unlimited)

While a full evaluation will have to await further study, in general it seems to distinguish person names from company names reasonably reliably, and it seems to have discovered that person names consist of a first name (A0), a middle name or initial (A2), a surname (A3) and an optional suffix (A4). Similarly, it seems to have uncovered that company names typically end in a phrase such as inc, ltd or co.

8 Conclusion

This paper establishes a connection between two very different kinds of probabilistic models; LDA models of the kind used for topic modelling, and PCFGs, which are a standard model of hierarchical structure in language. The embedding we presented shows how to express an LDA model as a PCFG, and has the property that Bayesian inference of the parameters of that PCFG produces an equivalent model to that produced by Bayesian inference of the LDA model’s parameters.

The primary value of this embedding is theoretical rather than practical; we are not advocating the use of PCFG estimation procedures to infer LDA models. Instead, we claim that the embedding suggests novel extensions to both the LDA topic models and PCFG-style grammars. We justified this claim by presenting several hybrid models that combine aspects of both topic models and
grammars. We don’t claim that these are necessarily the best models for performing any particular tasks; rather, we present them as examples of models inspired by a combination of PCFGs and LDA topic models. We showed how the LDA to PCFG embedding suggested a “sticky topic” model extension to LDA. We then discussed adaptor grammars, and inspired by the LDA topic models, presented a novel topic model whose primitive elements are multi-word collocations rather than words. We concluded with an adaptor grammar that learns aspects of the internal structure of proper names.

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