Dynamical Masses of the Primary Be Star and Secondary sdB Star in the Single-lined Binary \( \kappa \) Dra (B6 IIIe)

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Received 2022 September 5; revised 2022 October 5; accepted 2022 October 6; published 2022 November 23

Abstract

Because many classical Be stars may owe their nature to mass and angular-momentum transfer in a close binary, the present masses, temperatures, and radii of their components are of high interest for comparison to stellar evolution models. Object \( \kappa \) Dra is a 61.5 day single-lined binary with a B6 IIIe primary. With the CHARA Array instruments MIRC/MIRC-X and MYSTIC, we detected the secondary at (approximately photospheric) flux ratios of 1.49\% ± 0.10\% and 1.63\% ± 0.09\% in the \( H \) and \( K \) band, respectively. From a large and diverse optical spectroscopic database, only the radial velocity curve of the Be star could be extracted. However, employing the parallaxes from Hipparcos and Gaia, which agree within their nominal 1\( \sigma \) errors, we could derive the total mass and found component masses of 3.65 \pm 0.48 and 0.426 \pm 0.043 \( M_\odot \) for the Be star and the companion, respectively. Previous cross-correlation of the observed FUV spectrum with O-type subdwarf (sdO) spectral model templates had not detected a companion belonging to the hot sdO population known from \( \sim \)20 earlier-type Be stars. Guided by our full 3D orbital solution, we found a strong cross-correlation signal for a stripped subdwarf B-type companion (FUV flux ratio of 2.3\% ± 0.5\%), enabling the first firm characterization of such a star and making \( \kappa \) Dra the first mid- to late-type Be star with a directly observed subdwarf companion.

**Unified Astronomy Thesaurus concepts:** Be stars (142); Multiple star evolution (2153); O subdwarf stars (1138); B subdwarf stars (129); Optical interferometry (1168); Orbit determination (1175)

Supporting material: figure sets

1. Introduction

The Be stars are extremely rapidly rotating and nonradially pulsating B-type stars of luminosity classes V, IV, and III that possess self-ejected, gaseous disks with \( \sim \)Keplerian rotation (Rivinius et al. 2013). They constitute about 15\%–20\% of all B-type stars in the local Galactic environment (Rivinius et al. 2013). From a stellar evolution perspective, a significant fraction of Be stars are thought to be products of binary interaction and mass and angular-momentum exchange between two initial B-type stars, one of which expands while it evolves beyond the main sequence (MS; e.g., Pols et al. 1991; Shao & Li 2014, 2021). The mass transfer from the originally more massive component rejuvenates and spins up the mass gainer, which then becomes the classical Be star. The mass donor loses its envelope (and with it a large fraction of its initial mass), while the hot stripped core remains and is often referred to as an OB-type subdwarf star (sdOB). Further evolution of the system may result in a white dwarf (WD), neutron star (NS), or black hole (BH).

The hypothesis that a given Be star is a binary interaction product can be positively supported through (i) the detection of a stripped companion, (ii) the identification of single Be stars as binary merger products, or (iii) runaway stars from a former binary disrupted in a supernova explosion. On the other hand, it can be ruled out by detecting a close stellar companion that is still on the MS; this would prove that Be stars can acquire their properties as a consequence of the initial formation conditions (Martayan et al. 2007; Hastings et al. 2020) and/or internal structural changes during their MS lifetimes (Ekstrom et al. 2008; Granada et al. 2013). Finding a truly single Be star that is not a binary interaction product would lead to the same conclusion. However, the presence of very faint and low-mass companions such as WDs or sdOBs is difficult to rule out with current observational means (see the case of the Bn star Regulus with a pre-WD companion; Gies et al. 2020). Mass transfer products such as Be stars could also be identifiable as blue stragglers, i.e., stars likely rejuvenated by mass transfer, in stellar clusters (Bodensteiner et al. 2021). Furthermore, since
most Be stars are nonradial pulsators, long-term monitoring by space photometry can place tight limits on orbital Doppler shifts of the pulsation frequencies (see Baade et al. 2018a, and references therein). The method is most promising for early-type Be stars, in which $p$-mode frequencies are found that are relatively isolated and both higher and more stable than the others (Labadie-Bartz et al. 2022) so that they require shorter observing time spans. For current facilities, these time spans are too long, but they may be within reach of PLATO (Rauer et al. 2014). So far, no model has claimed exclusiveness in its explanation of Be stars, although binary products have been positively identified in many cases.

Currently, about 20 Be stars are known to have stripped companions, most of which were confirmed with far-UV (FUV) spectroscopy, as it is in the FUV where the flux ratios are most favorable (Wang et al. 2021; Klement et al. 2022, and references therein). All of the spectroscopic FUV detections were found to be compatible with the sdO nature of the companions, while no firm case of a cooler sdB companion has been presented as of yet. There are also more than 160 confirmed and candidate Be X-ray binaries (BeXRBs; Raguzova & Popov 2005), which are mostly Be+NS systems that probably evolved in a similar fashion as the Be+sdO binaries but from more massive progenitor systems (Reig 2011). The Be primaries occupy a narrow range between O9 and B2 in that probably evolved in a similar fashion as the Be references therein an early A-type dwarf companion on a 7 yr orbit, appears to be 12 List updated athttp://xray.sai.msu.ru/~raguzova/BeXcat/.

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broadened line profiles. In $\kappa$ Dra, the main variability with a reported period of 0.545 days concerns line width and symmetry and was attributed to a low-order NRP mode (Hill et al. 1991).

As in many other Be stars, longer-term variations in $\kappa$ Dra concern the ratio in strength of the violet ($V$) and red ($R$) peaks of prominent emission lines. These $V/R$ variations are phase-locked to the orbital period (Saad et al. 2005) and, as in other Be binaries, probably originate from a two-armed ($m = 2$) density wave in the disk excited by the companion (Panoglu et al. 2018).

In addition, $\kappa$ Dra exhibits long-term variations in the strength of its emission lines, which have been reported to grow and dissipate with a cycle length of around 22 yr (Juza et al. 1994; Saad et al. 2004). In earlier-type Be stars (but see also the case of the B7–8 IIe star $\kappa$ Pup: Baade et al. 2018a), such cyclic behavior—but on shorter timescales—has been seen linked to the interplay of multiple NRP modes (Baade et al. 2018b). Currently, $\kappa$ Dra is in an almost diskless phase, and, according to the mentioned cyclic behavior, the emission is expected to regain strength in the near future.

In this new study of $\kappa$ Dra, we combine new radial velocities (RVs) from high-resolution spectroscopy with new astrometric measurements from optical long-baseline interferometry (Section 2). The goals are the determination of the 3D binary orbit of $\kappa$ Dra (Section 3), a discussion of the fundamental parameters of the primary Be star, and a characterization of the nature of the companion (Section 4). After a concise summary, Section 5 develops the conclusions, as well as goals for future observations.

2. Observations

2.1. Hipparcos and Gaia Astrometry

The parallax measurements for $\kappa$ Dra from the Hipparcos (ESA 1997; van Leeuwen 2007) and Gaia (Gaia Collaboration et al. 2016, 2018, 2021) space missions are in good mutual agreement. The re-reduction of the Hipparcos astrometry by van Leeuwen (2007) should supersede the original reduction, which also considered a single-star solution for $\kappa$ Dra, although the resulting parallaxes agree well within the formal errors. The distances derived from the Hipparcos re-reduction, Gaia Data Release 2, and Gaia Data Release 3 (DR3) catalogs amount to 150.4$^{+8.1}_{-7.3}$, 140.1$^{+6.8}_{-6.2}$, and 142.7$^{+6.3}_{-5.8}$ pc, respectively (formal parallax errors are the only uncertainties considered here).

Further inspection of the Gaia DR3 data reveals that, with a value of 2.441, the quality flag “renormalized unit weight error” (RUWE) exceeds the threshold of 1.4, above which astrometric solutions are considered degraded (Lindegren et al. 2021). Therefore, it appears that the submilliarcsecond orbital motions of the primary Be star in $\kappa$ Dra (reported in Section 3.1) are appreciably affecting the Gaia astrometric solution. Alternatively, the astrometric solution could be degraded due to detector saturation ($\kappa$ Dra is very bright at $G = 3.9$) or variability in the circumstellar environment. In any case, it was found that for RUWE < 3, the astrometric solution can still be useful within the uncertainties (Maíz Apellániz et al. 2021), and since the agreement between Hipparcos and the individual Gaia releases is good, we adopt the Gaia DR3 parallax and proper motions for the purposes of this study.

The proper motion of $\kappa$ Dra according to Gaia DR3 (Gaia Collaboration et al. 2021) is in good agreement with that measured by Hipparcos (van Leeuwen 2007), and there are no indications of a proper-motion anomaly indicating orbital motions on long timescales (Kervella et al. 2019, 2022a). The peculiar tangential velocity, obtained after subtracting the Sun’s peculiar motion (Schonrich et al. 2010) and differential Galactic rotation (Moffat et al. 1998, 1999), is $26.7 \pm 1.2$ km s$^{-1}$. The peculiar space velocity calculated from the systemic velocity of $\kappa$ Dra determined in this work (see Section 3.3) is $33.8 \pm 1.2$ km s$^{-1}$. These values are in good agreement with those previously determined on the basis of Hipparcos (Berger & Gies 2001). Even though the space velocity is close to the threshold of 40 km s$^{-1}$ typically considered for runaway stars (Blaauw 1961), $\kappa$ Dra is a close noneccentric binary (Section 3.3) with a noncompact companion; therefore, the runaway status bears no significance to the origin of the Be star nature of the primary star.

2.2. Photometry and Spectrophotometry

2.2.1. Spectral Energy Distribution

For the basic fitting of the spectral energy distribution (SED), we used the data set collected by Klement et al. (2019) and complemented it with flux-calibrated UV spectra from the IUE (Boggess et al. 1978) and near-IR photometry measured by Dougherty et al. (1991). A total of 32 IUE spectra were retrieved from the INES database. They were selected to have been taken with the large aperture to ensure reliable flux calibration, but two clear outliers had to be discarded (SWP 29665 and LWP 8089). In fact, SWP 29665 appears to be a misidentified spectrum of the Be binary 59 Cygni because it has the same appearance as others of 59 Cygni, and a cross-correlation function (CCF) analysis with a hot 45 kK template reveals the spectral signature of the hot companion at the predicted velocity (Peters et al. 2013) for the date of the observation.

The other sources of SED data include the HPOL spectropolarimeter (Davidson et al. 2014), the Simbad database (Wenger et al. 2000), and the catalogs of the IR space missions IRAS (Beichman et al. 1988; Joint Iras Science 1994), WISE (Wright et al. 2010; Cutri et al. 2021), and AKARI/IRC (Ishihara et al. 2010a, 2010b).

2.3. Near-IR Interferometry

Near-IR long-baseline interferometry was secured at the Center for High Angular Resolution Astronomy (CHARA) Array (ten Brummelaar et al. 2005; Schaefer et al. 2020) with the beam combiner MIRC (Monnier et al. 2006) and its upgraded successor, MIRC-X (Anugu et al. 2020). MIRC-X is an image-plane beam combiner operating in the H band at low spectral resolving powers of 50, 100, or 190, resulting in interferometric fields of view (FoVs) of $\sim$50, $\sim$100, and $\sim$200 mas, respectively. In combination with the six CHARA 1 m telescopes and long baselines of up to $\sim$330 m, MIRC-X achieves an angular resolution of down to $\sim$0.5 mas and very good coverage of the $(u, v)$ plane even with snapshot

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13 http://sdc.cab.inta-csic.es/cgi-inex/UE/EdbsMY
14 http://www.sal.wisc.edu/~pol/
15 http://simbad.u-strasbg.fr/simbad/
16 https://irsa.ipac.caltech.edu/IRASdocs/iras.html
17 https://www.nasa.gov/mission_pages/WISE/main/index.html
18 https://www.isas.jaxa.jp/en/missions/spacecraft/past/akari.html
observations. Among many other science cases, these properties enable efficient detection of binary companions to bright \( (H \lesssim 7.5) \) stars with contrast ratios as high as 1:500. The MIRC-X twin instrument MYSTIC (Setterholm et al. 2022) has operated at CHARA simultaneously with MIRC-X in the near-infrared \( K \) band (with default \( R = 49 \) corresponding to an interferometric FoV of \( \sim 65 \) mas) since 2021 August.

Using different spectral modes, \( \kappa \) Dra was observed on 6 nights in 2012, 2013, and 2021 (Table 1). On a single night in 2021 (2021 December 18), both MIRC-X and MYSTIC data were obtained simultaneously. The star occupies a position in the sky for which six-telescope delay-line operation is not available at CHARA; thus, all of the data sets were obtained in five-telescope mode, i.e., with 10 individual baselines (telescope pairs) and 10 closed triangles (of which only five are independent). Accordingly, each interferometric observation resulted in 10 sets of squared visibilities (VIS2) and 10 sets each of closure phases (CPs) and triple amplitudes (T3AMP). The data were reduced using the dedicated pipelines for MIRC\(^{19} \) (Monnier et al. 2007) and MYSTIC-X/MYSTIC\(^{20} \) (pipeline version 1.3.5; Anugu et al. 2020). Some data sets required the removal of edge spectral channels due to a highly degraded signal-to-noise ratio (S/N).

Calibrator observations were obtained before and/or after the science target and used to correct for atmospheric and instrumental effects in the raw measurements to obtain absolute-calibrated VIS2, CP, and T3AMP. The calibrators were selected using the SearchCal software\(^{21} \) (Chelli et al. 2016) and are listed along with their uniform disk (UD) diameters in Table 2. The calibrator diameters were adopted from the JMMC catalog of stellar diameters (Bourgés et al. 2014, 2017).

The absolute calibration of VIS2 and T3AMP is more susceptible to atmospheric turbulence than that of CP, as the latter is a differential measurement explicitly designed to cancel the turbulence-induced terms in the interferometric phase. Unfortunately, several of our epochs were affected by bad atmospheric conditions; a combination of poor seeing, spikes in humidity, and/or wind gusts made for unstable fringes on 2012 April 28, 2021 March 6, 2021 May 20, and, to a lesser extent, 2021 December 18. While the CP precision turned out to be sufficient even on these nights, VIS2 and T3AMP had to be completely discarded for the three most affected ones. For 2021 December 18, VIS2 and T3AMP had to be discarded from the MIRC-X part of the data set, while the MYSTIC part could be used in full. The calibrated OIFITS files corresponding to all MIRC(-X) and MYSTIC observations analyzed in this work will be available in the Optical Interferometry Database\(^{22} \) (Haubois et al. 2014) and the CHARA Data Archive.\(^{23} \)

### 2.4. Optical Spectroscopy

We assembled over 500 individual spectra from the archives of various spectrographs, as well as from the database of Be star spectra mostly taken by amateur astronomers, BeSS\(^{24} \) (Neiner et al. 2011). Heliocentric correction was applied to the wavelength scale of all spectra, and all dates were converted to heliocentric Julian dates (HJD). A significant number of the spectra were originally obtained for spectropolarimetric purposes and to study short-term line profile variations. Therefore, these data sets cluster in a few nights each and have a high S/N. A subset of 15 HEROS blue and 15 HEROS red spectra was previously analyzed by Saad et al. (2004, 2005, 2021). The basic properties of the spectra, including the resolving power, S/N, and spectral coverage, are summarized in Table 3, and the spectrographs are briefly introduced in the following.

BeSS. The available echelle spectra include professional spectra from MUSICOS, as well as amateur spectra taken with different instruments. MUSICOS was a fiber-fed spectrograph for multisite observations (Baudrand & Bohm 1992). The quality of these spectra varies, and their wavelength calibration might be unreliable.

ELODIE. This was an echelle spectrograph installed at the Observatoire de Haute-Provence 1.93 m reflector in southeastern France (Baranne et al. 1996). Two ELODIE spectra were recovered from the archive\(^{25} \) (Mouttaka et al. 2004).
Table 3  
Spectroscopic Data Sets

| Instrument/Detector | Telescope        | MJD      | Number | Resolving Power | S/N | Spectral Coverage (Å) |
|---------------------|-----------------|----------|--------|-----------------|-----|-----------------------|
| BeSS database       | Multiple        | 54,904–56,494 | 91     | ~11,000         | 100–400    | 4300–6900              |
| ELODIE              | OHP 1.9 m       | 51,570–51,572 | 2      | 42,000          | 300–400    | 3850–6800              |
| ESPaDOnS            | CFHT 3.6 m      | 53,512–55,229 | 104    | 68,000          | 400–500    | 3700–10980             |
| FLASH               | Tautenburg 2.0 m | 48,261–48,443 | 195    | 12,000           | 100–400    | 4050–6780              |
| FLASH2              | Wendelstein 80 cm | 51,680–51,757 | 21     | 20,000           | 100–400    | 4050–6780              |
| HEROS blue          | Ondřejov 2.0 m  | 51,899–52,714 | 45     | 20,000           | 100–300    | 3500–5500              |
| HEROS red           | Ondřejov 2.0 m  | 51,899–52,714 | 53     | 20,000           | 100–300    | 5600–8600              |
| SWP                 | IUE             | 43,953–48,191 | 24     | 7500             | 20        | 1150–1980              |
| LWP/LWR             | IUE             | 43,953–47,272 | 6      | 12,500           | 20        | 1850–3350              |
| MUSICOS             | TBL 2.0 m       | 51,897–52,265 | 26     | 35,000           | 300–500    | 3800–8700              |
| Narval              | TBL 2.0 m       | 54,105–55,949 | 64     | 65,000           | 400–600    | 3700–10050             |

Table 4  
Relative Astrometric Positions of the Companion

| HJD−2,400,000.5 | ρ (mas) | PA (deg) | Δ.R.A. (mas) | Δ.Decl. (mas) | σ-a (mas) | σ-b (mas) | σ-PA (deg) | f (% primary) | UD Diam. (mas) | Band |
|-----------------|--------|----------|-------------|--------------|----------|----------|-----------|-------------|--------------|------|
| 56,045,206      | 3.370  | 287,994  | −3.208      | 1.042        | 0.045    | 0.029    | 94.6      | 1.29 ± 0.08  | 0.45*         | H    |
| 56,410,253      | 3.406  | 307,222  | −2.712      | 2.060        | 0.054    | 0.045    | 112.6     | 1.22 ± 0.13  | 0.45 ± 0.02   | H    |
| 59,279,510      | 3.213  | 97,733   | 3.183       | −0.433       | 0.023    | 0.019    | 158.2     | 1.33 ± 0.06  | 0.354*        | H    |
| 59,354,234      | 2.468  | 0.971    | 0.040       | 2.458        | 0.044    | 0.042    | 86.1      | 1.6 ± 0.3    | 0.354*        | H    |
| 59,377,197      | 2.594  | 247,518  | −2.397      | −0.992       | 0.031    | 0.016    | 127.2     | 1.59 ± 0.09  | 0.354 ± 0.004 | H    |
| 59,566,509      | 2.180  | 210,292  | −1.100      | −1.882       | 0.037    | 0.017    | 205.6     | 2.01 ± 0.13  | 0.354*        | H    |
| 59,566,509      | 2.228  | 211,400  | −1.161      | −1.902       | 0.048    | 0.019    | 135.9     | 1.49 ± 0.10  | 0.405 ± 0.016 | K    |

Note. Here ρ is the angular separation between the components; PA is the position angle (from north to east); Δ.R.A. and Δ.decl. are the companion coordinates relative to the primary; σ-a and σ-b are the major and minor axes of the error ellipse, respectively; σ-PA is the position angle of the error ellipse (from north to east); f is the secondary-to-primary flux fraction; and UD diam. is the diameter of the primary (including any contribution from the disk).

* Fixed.

ESPaDOnS/Narval. ESPaDOnS26 (Donati 2003; Donati et al. 2006; Wade et al. 2016) and Narval27 (Wade et al. 2016) are twin instruments with spectropolarimetric capabilities. Data from these instruments are the best-quality spectroscopic data sets available for κ Dra.

FLASH/HEROS/FLASH2. The Fiber-Linked Astronomical Spectrograph of Heidelberg (FLASH; Mandel 1988) was a portable fiber-linked echelle spectrograph with a single camera. The Heidelberg Extended Range Optical Spectrograph (HEROS28; Kaufer 1998; Stefl & Rivinius 2000) was an upgrade of FLASH with a thinner fiber (and hence higher spectral resolution) and two spectral channels (blue and red). FLASH2 was a phase of FLASH with the thinner fiber but when the blue camera was out of commission and the wavelength range was adjusted for observation with the red arm only. Descriptions of these instruments and the reduction procedure can also be found in Rivinius et al. (2001) and references therein.

3. Orbital Analysis

3.1. Measurement of the Astrometric Positions of the Companion from Interferometry

We fitted geometric models to the interferometric data with the open-source Python code Parametric Modeling of Optical InteRferomEtric Data (PMOIRED29; Mérand 2022). This is an analysis tool for interferometry, which relies on semianalytical expressions for complex visibilities to construct geometrical models made from building blocks such as UDs and Gaussians. For the companion detection, we used the dedicated open-source Python code Companion Analysis and Non-Detection in Interferometric Data (CANDID30; Gallenne et al. 2015), which includes corrections for the effect of bandwidth smearing on the derived flux ratios. The uncertainties of the fitted parameters were determined using a data resampling (bootstrapping) algorithm and include the instrumental wavelength calibration uncertainty of 0.5% (Anugu et al. 2020).

The κ Dra binary system was first represented by a UD for the Be primary (including its disk) and a point source for the secondary. A grid search with CANDID was used to find the relative position (Δ.R.A., Δ.decl.) and relative flux f of the secondary (expressed as a percentage of the primary flux) for each epoch. For the epochs with available VIS2 and T3AMP, the primary UD diameter was included as a free parameter, while it was kept fixed for the others. The companion was successfully detected, its position was determined for all seven data sets, and the results are summarized in Table 4. It should be noted that the χ2 map resulting from the grid search of the MYSTIC data set—when using only the CP—shows two minima of an equal depth. While one of the minima agrees with the corresponding MIRC-X position and is close to the MIRC-X flux ratio, the other is clearly offset at double the separation and flux ratio. Consequently, we adopt the former position as the correct one. The binary fit to the best-quality data set (MJD 59,377.197) is

26  http://www.ast.obs-mip.fr/projets/espadons/espadons.html  
27  http://www.ast.obs-mip.fr/projets/narval/  
28  https://www.lsw.uni-heidelberg.de/projects/instrumentation/Heros/  
29  https://github.com/amerand/PMOIRED  
30  https://github.com/amerand/CANDID, https://github.com/agallenne/GUCandid
shown in Figure 1, while the plots with the final fits to all seven data sets are available in the online journal.

The resulting UD diameter values in the $H$ band show an apparent decrease in size between 2013 and 2021 and a larger size in the $K$ band relative to the $H$ band in 2021. The $H$-band flux ratios indicate an increase from 2012/2013 to 2021 when comparing the corresponding averages ($1.25\% \pm 0.08\%$ and $1.63\% \pm 0.09\%$), as well as only the best epochs with complete data sets ($MJD 56,410.253$ and $59,377.197$). Finally, the flux ratio in the $K$ band is slightly lower than the average $H$-band flux ratio in 2021, although they agree within the error bars. The apparent decrease in size coupled with a small increase in the relative flux of the companion most likely reflects the significant disk dissipation that occurred between 2013 and 2021, as evidenced by the decreasing line emission in the spectra (Figure 2). The larger size in the $K$ band probably reflects what is expected for Be star disks due to the increasing free–free and bound–free opacity in ionized, gaseous environments (Vieira et al. 2015), i.e., the disk appearing larger at longer wavelengths, although the line emission from the dissipating disk was already very low at this time. The lower flux ratio in the $K$ band relative to the $H$ band points toward a companion that is hotter than the primary Be star, although the higher excess emission from the remaining disk could also contribute to the same effect.

With the companion positions determined for each epoch, we used PMOIRED to include an additional model component, an inclined Gaussian, to represent the circumstellar disk of the primary Be star and attempted to constrain its parameters by fitting the three full data sets. The UD component now representing the Be star photosphere was fixed at the near-photospheric measured diameter of 0.354 mas. Only the recent better-quality MIRC-X and MYSTIC data resulted in a constrained inclination and position angle (PA) of the Gaussian disk component (Table 5), although the overall fit to the data is not significantly improved. This suggests that these parameters are not constrained well by the data, most likely due to the fact that the disk had almost dissipated by 2021.

3.2. RV Measurements in Spectra

The spectrum of $\kappa$ Dra is dominated by rotationally broadened absorption lines from the primary B6 IIIe component. It is overlaid with generally double-peaked emission lines originating from the circumstellar disk; their separations are consistent with an intermediate-to-low inclination. No lines attributable to the secondary component are visible. The rotational broadening and variability of the line profiles due to NRPs hinder the accuracy of RV measurements of the primary component that would be achievable for stars with narrow and invariant lines. Since the disk of $\kappa$ Dra is not viewed close to edge-on and the line of sight does not intersect the disk, there are no narrow shell absorption lines that could be used as a proxy of the stellar RV. Nevertheless, using a large amount of spectra and measuring the RVs separately from
several different lines should alleviate possible systematic errors in the RV measurements, as the effects of the rapid variability should average out and only lead to possibly increased scatter.

Therefore, for the purpose of precise RV determinations of the primary Be star, we searched for prominent absorption lines uncontaminated by line emission from the disk and without other obvious circumstances affecting the line shape. Five lines were finally selected following careful inspection: He I λ4026, He I λ4471, Mg II λ4481, He I λ4713, and He I λ6678. Even though Mg II λ4481 and He I λ6678 are in hotter Be stars often contaminated by emission from the disk, in the case of κ Dra, there appears to be no emission component in these lines. After normalization of the surrounding continuum, the line profiles were fitted with a Gaussian profile to determine the RV shift at each epoch. Each measurement was visually checked, and poor fits resulting in clear outliers were discarded. With the exception of He I λ4713, all of the selected lines are affected by blends with forbidden transitions of unknown strength, so that the systemic velocity can be most accurately determined from this line (Underhill & Doazan 1982).

The spectroscopic data sets used in this study are of heterogeneous quality. The 168 spectra from ESPaDOnS and Narval have the highest quality, resolution, and S/N and yield the most precise RV measurements. The ELODIE data set is the second best in terms of spectra quality, but only two spectra are available. The 25 observations with MUSICOS and the 91 amateur spectra from the BeSS database have comparable resolution to those mentioned above; however, the spectral calibration may be less reliable, as MUSICOS was not optimized for this purpose, and the quality control of the BeSS data reduction procedures may be less stringent. The advantage of the BeSS spectra is that they are more uniformly distributed with orbital phase than the other data sets. The FLASH/HEROS/FLASH2 spectra are only partly usable for RV measurements due to a much lower resolution. Following an exploration of the influence of discarding lower-quality spectra on the resulting scatter, we conservatively discarded all RV measurements from spectral segments with S/N < 200 per resolution element. This

| HJD−2,400,000.5   | i (deg) | PA (deg) | Band |
|-------------------|---------|----------|------|
| 59,377.197        | 40.5 ± 5.1 | 133.0 ± 5.8 | H    |
| 59,566.509        | 34.2 ± 9.8 | 119 ± 18    | K    |

**Figure 2.** Top: Hα line profiles recovered from the BeSS spectral database. The colors correspond to dates as shown in the bottom panel. Bottom: equivalent width (EW) measured for all Hα profiles. A continuous decrease in emission strength is apparent from around 2010 and still ongoing. Vertical lines show the epochs of our interferometric observations.

**Table 5** Parameters of the Disk around the Be Star
resulted in a significant reduction of useful spectra for the lower-quality data sets from BeSS and FLASH.

For each instrument of origin, the scatter of individual RV measurements at similar epochs was used to estimate their $1\sigma$ uncertainties. As expected from the data quality, the scatter is the lowest for ESPaDOnS and Narval and increases by a factor of 2–3 for the other data sources. The following values were finally adopted: 3 km s$^{-1}$ for ESPaDOnS/Narval, 6 km s$^{-1}$ for ELODIE, and 9 km s$^{-1}$ for the remaining instruments.

### 3.3. Orbital Solution

The orbital solution was obtained using the code FOTEL (Hadrava 2004), which can combine various data sets, such as photometry (for eclipsing binaries), RVs (for spectroscopic binaries), and astrometric orbital positions (for astrometric/interferometric binaries). In the case of $\kappa$ Dra, we combined the RVs measured in the spectra with the astrometric positions measured from near-IR interferometry. For the weights of individual measurements, required for the orbital solution by FOTEL at input, the inverse of the corresponding measurement uncertainties was adopted. To ensure equal influence of the astrometry and the RVs, the relative weight of the two measurement sets was adjusted so that they contributed approximately equal amounts to the total residuals.

In addition to the stellar coordinates and proper motion (Section 2.1), a full dynamical description of a binary system requires the knowledge of 10 parameters. Four of these—the period ($P$), the epoch of periastron passage ($T_0$), the eccentricity ($e$), and the longitude of periastron ($\omega$)—can be determined independently from both the astrometry and the RVs. On the other hand, only the RVs are sensitive to the line-of-sight velocities, i.e., the velocity semiamplitudes of the two components ($K_1, K_2$) and the systemic velocity ($\gamma$), while astrometry is the only source of information about the orbital inclination ($i$), the PA of the line of nodes ($\Omega$, although RVs are needed to distinguish the ascending and descending nodes), and the angular semimajor axis of the orbit ($a_\alpha$; e.g., Batten 1973).

With measurements of all 10 parameters, the absolute size of the orbit ($a$) can be calculated from the $K$ semiamplitudes, $i$, and $P$, while the distance to the system ($D$) from a comparison of the absolute and angular size of the orbit, and, finally, the mass of the system from the third Kepler law. The masses of the individual components ($M$) are then found from the ratio of the $K$ semiamplitudes. This ideal case corresponds to an astrometric binary that is also an SB2, where it is possible to obtain the $K$ semiamplitudes of both components from composite spectra. For $\kappa$ Dra, however, which is an SB1, an independent measurement of the distance $D$ is not possible, and for the determination of the component masses, we have to rely on the parallax measurement (Section 2.1).

In the first solution, we only used the best-precision RVs from ESPaDOnS and Narval—a total of 839 from all five spectral lines (Section 3.2)—alongside the astrometry. Fixing $e = 0$ to enforce a circular orbit favored by earlier studies (Section 1; Table 6) gave a good fit to both data sets and a well-constrained set of orbital parameters. Adding $e$ and $\omega$ as free parameters did not result in an elliptic orbit, so the data are compatible with an infinitesimally low eccentricity and undefined $\omega$. The binary parameters obtained are listed in the first column of Table 6, where they are also compared to the results from older spectroscopic studies, showing very good agreement in the period ($P$) and good agreement in the RV semiamplitude of the Be star ($K_{\text{Be}}$). The rms of the $(O-C)$ residuals of the ESPaDOnS and Narval RV measurements is 2.6 km s$^{-1}$.

In the next step, we included the full set of 1850 individual RV measurements. As expected, the combined RV curve shows considerable scatter for the lower-quality data sets. More specifically, the MUSICOS measurements in the He I $\lambda$4713 line are systematically offset to positive values by about 15 km s$^{-1}$. To a smaller extent, the BeSS spectra (with mostly even phase coverage) show an offset to negative values for the He I $\lambda$4471 line, while HEROS appears offset to positive values. However, since these systematics were limited to only these few instances and for lower-weighted measurements, they were not excluded from the solution. The resulting orbital parameters from the full data set agree to within $1\sigma$ of the first solution, while the uncertainty of $K_{\text{Be}}$ slightly increased. Thus, the first solution using ESPaDOnS and Narval only is adopted as the final solution (Table 6). The final RV curve with RV measurements from He I $\lambda$4026 is plotted in Figure 3. The full set of five figures with RV measurements from all five spectral lines is available in the online journal.

The astrometric orbit obtained is shown in Figure 4. While there are only seven astrometric data points, the number of parameters constrained exclusively by the astrometry is only three—$i$, $a_\alpha$, and $\Omega$—so the size of the data set is sufficient for the orbital solution. The median $(O-C)$ of the astrometric points is 76 $\mu$as, which is reasonable considering the high contrast resulting in the CP signal close to zero and the inability to fully use the other interferometric observables to constrain the companion position.

The orbital inclination is $130^\circ \pm 3^\circ 4$, indicating a projected motion from north through west, which is the clockwise direction in Figure 4. The inclination of the circumstellar disk should then be close to $40^\circ$ if the orbital and disk planes are aligned. The results from the disk fitting are consistent with this value, and the PA of the disk agrees well with $\Omega$ determined from the orbital solution (Table 5). The resulting masses are discussed in Section 4.

### 4. Fundamental Parameters and Nature of the Companion

For the Be primary star, Frémat et al. (2005) derived $T_{\text{eff}} = 13,982 \pm 392$ kK and $\log g = 3.479 \pm 0.061$ by fitting model atmospheres accounting for rapid rotation and gravitational darkening. Touhami et al. (2013) fitted a Kurucz model spectrum (Kurucz 1979) with these parameters to UV spectra (IUE) to derive the limb-darkened disk (LD) diameter ($0.385 \pm 0.011$ mas) and interstellar reddening ($E(B-V) = 0.022 \pm 0.008$ mag). The LD diameter was converted to a UD diameter of $0.381 \pm 0.011$ mas using the linear limb-darkening parameter from Claret & Bloemen (2011) and stellar parameters listed by Touhami et al. (2013). The UD diameter compares well with the interferometrically measured $H$-band UD diameter in an almost diskless state, which equals $0.354 \pm 0.004$ (Section 3.1). However, since that measurement comes from a single calibrated interferometric bracket, the result is not very robust, so in the following, we use the former value determined from fitting the FUV spectrum. The average physical radius of $\kappa$ Dra implied by the Gaia DR3 distance is then $R_{\kappa\text{dra}} = 5.85 \pm 0.18$ $R_\odot$. From the above estimates of $R_{\kappa\text{dra}}$ and $T_{\text{eff}}$ for the primary Be star, the luminosity $L$ is $1178 \pm 151 L_\odot$. The absolute $V$-band magnitude $M_V$ is $-1.95 \pm 0.40$ mag resulting from the apparent magnitude $m_V$ of...
The dynamical mass of the Be primary star obtained from the orbital parameters and Gaia DR3 distance is 3.65 ± 0.48 \( M_\odot \) (Section 3.3, Table 6). Comparing this value with the typical masses of slowly rotating stars with similar \( T_{\text{eff}} \) and spectral type (B6) reveals that the mass of \( \kappa \) Dra is slightly lower than expected. For instance, Harmanec (1988) gives a mass range for B6 stars of 3.63–3.93 \( M_\odot \), with a mean of 3.78 \( M_\odot \), based on observed masses of 15 eclipsing binaries. Later compilations of masses of eclipsing binaries give still somewhat higher masses for stars with similar \( T_{\text{eff}} \); e.g., the secondary B6V component of U Oph has a mass of 4.58 ± 0.05 \( M_\odot \).\(^{31}\) (Southworth 2015).

Relying on spectrophotometry and Hipparcos parallaxes, Hohle et al. (2010) derived a median mass of 4.65 ± 0.72 for B6 III stars. As for the radius, \( R_{\text{Be}} = 5.85 ± 0.18 \ R_\odot \) corresponds to the equatorial radius, which is larger than the polar radius due to the rapid rotation. In the case of critical rotation, the polar radius is \( R_p = \frac{2}{3} R_{\text{Be}} = 3.90 ± 0.12 \ R_\odot \), i.e., still significantly higher than the typical radius of B6 stars derived from eclipsing binaries, which is ~3.05 \( R_\odot \) (Harmanec 1988).

As a crucial constraint for the nature of the companion, Wang et al. (2017) found from IUE spectra that the FUV photospheric flux ratio \( f_{\text{phot,FUV}} \) of a possible sdO companion has to be less than 1.0% for the sdO star to remain undetected. Combining this information with the measured dynamical mass and the near-IR flux ratio then enables the characterization of the companion. To make use of the measured flux ratio, the contribution of the circumstellar disk (very small in 2021) should be taken into account. Estimating the exact values for the continuum contribution of the disk from the observed line emission is beyond the scope of this work, so the average flux ratio measured in 2021 (1.63% ± 0.09% in the H band) is taken as the photospheric flux ratio between the components \( f_{\text{phot,H}} = f_{\text{comp,phot,H}}/f_{\text{Be,phot,H}} \), neglecting the small contribution from the disk. Below, we consider the better-constrained H-band flux ratio, but the results are compatible when using the slightly lower K-band flux ratio.

In order to attempt to identify the nature of the companion, we used Kurucz/Castelli spectra\(^{32}\) (Castelli & Kurucz 2003) to represent both the primary Be star (\( T_{\text{eff}} = 13,982 \) kK, \( \log g = 3.479 \), and \( R_{\text{Be}} = 5.85 \ R_\odot \)) and the companion (Figure 5). The model spectra of the companion were renormalized to the measured companion flux in the H band and chosen to represent either a stripped sdOB star or an MS star to obtain the expected flux ratio in the FUV \( f_{\text{phot,FUV}} \). This procedure also leads to an estimate of the radius of the companion, providing an additional constraint for the nature of the companion. This is done by comparing the surface fluxes from the Kurucz/Castelli models, which at the given \( T_{\text{eff}} \) would contribute the observed flux fraction in the H band, \( f_{\text{phot,H}} = f_{\text{comp,phot,H}}/f_{\text{Be,phot,H}} \), neglecting the small contribution from the disk. Below, we consider the better-constrained H-band flux ratio, but the results are compatible when using the slightly lower K-band flux ratio.

First, values for \( T_{\text{eff}} \) of 25, 35, and 45 kK and \( \log g \) of 4.75 were used to represent an sdO companion. This results in an expected \( f_{\text{phot,FUV}} \) of ~10%, ~20%, and ~25%, respectively, which is clearly higher than the limit of 1% (Wang et al. 2017). For a cooler sdB companion with a \( T_{\text{eff}} \) of 15 and 20 kK (and \( \log g \) of 4.75), \( f_{\text{phot,FUV}} \) decreases to ~2.3% and ~5.5%, respectively. This implies that an sdO companion can be ruled out, while a cooler sdB remains a possibility, as the search in the FUV was optimized for an sdO rather than an sdB star.

Note.\(^4\) Determined from the He I \( \lambda 4713 \) line.

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3.89 mag (Ducati 2002), an adopted \( R_V \) of 3.1, and \( E(B-V) \) determined by Touhami et al. (2013). This is in agreement with the typical \( M_V \) for spectral types B6 IIIe to B8 IIIe, which are brighter by about 1.0–1.5 mag than the corresponding non-be stars of the same spectral types according to Wegner (2006).

However, it should be noted that in that work, the possible contribution from the disk was not accounted for, while it can amount to as much as ~0.5 mag (Labadie-Bartz et al. 2017). The \( \sin i \) of \( \kappa \) Dra is 200 ± 12 km s\(^{-1} \) according to Frémat et al. (2005).

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\(^{31}\) https://www.astro.keele.ac.uk/jkt/debcat/

\(^{32}\) https://www.stsci.edu/hst/instrumentation/reference-data-for-calibration-and-tools/astronomical-catalogs/castelli-and-kurucz-atlas
This means that the upper limit of $f_{\text{phot,FUV}}$ of 1% is probably too low in the case of an sdB companion. A late-type MS star could be a possibility, as its contribution to the FUV flux would be negligible. Using the values given by Pecaut & Mamajek (2013), the measured dynamical mass of the companion best corresponds to an M2V star. However, the resulting $R_{\text{comp}}$ for an M2V companion from Equation (1) is $2.1 R_\odot$, which is clearly too high for the expected radius of 0.446 $R_\odot$ (Pecaut & Mamajek 2013). Thus, an MS companion appears to be ruled out as well.

We can also rule out the possibility of the companion being a WD due to the intrinsically extremely low luminosities of these stars of the order of $\sim 10^{-2}$ to $\sim 10^{-4}$ $L_\odot$ (e.g., Giammichele et al. 2012). Even considering a bloated pre-WD, which would possibly have sufficient luminosity, would mean that it has to be much hotter than the primary, so the same arguments described above for a hot sdO are valid.

Given the evidence that the companion might be cooler than found for other stripped companions of Be stars, we re inspected the ultraviolet spectral results from IUE that led to the null detection reported by Wang et al. (2017). We followed the same method as before by forming CCFs in the wavelength range 1150–1950 Å of each spectrum with an assumed model template spectrum and then making a Doppler tomography reconstruction of the CCF components for the Be star and its companion. However, the new analysis differs in three ways from that of Wang et al. (2017). First, we omitted spectrum SWP 29665, which leaves a set of 24 IUE high-dispersion FUV spectra (see Section 2.2.1). Second, we adopted the improved orbital elements and mass ratio estimate from Table 6 to set the orbital velocities of the components used in the tomographic reconstruction. Finally, we used spectral model templates from the UVBLUE grid by Rodríguez-Merino et al. (2005; based upon the ATLAS9/SYNTH codes by Robert Kurucz) for $T_{\text{eff}} = 13–25$ kK, log $g = 5.0$, and solar metallicity.

This method using cooler model spectral templates reveals the spectral signature of the companion so that the companion is spectroscopically detected for the first time, and the validity of our orbital solution (Table 6) is confirmed. This also marks the first time that a stripped sdB companion to a Be has been
The FUV region, near-IR is shown as two dashed black horizontal lines signifying the edges of the derived band. The mid-IR power-law slope of the IR excess from the circumstellar disk (typical for Be stars) is shown as a dotted gray line. The reddened model spectrum for the sdB companion \( (T_{\text{eff}} = 16.7 \, \text{kK}, R = 0.69 \, R_\odot \) ) renormalized to the measured flux in the \( H \) band (neglecting the possible contribution from the dissipating disk; see text) is shown in purple. The FUV flux ratio of 2.3% \( \pm 0.5% \) determined from FUV spectra is shown as two dashed black horizontal lines signifying the edges of the derived confidence interval. From short to long wavelengths, the gray vertical bands indicate the FUV region, near-IR \( H \) band, and \( K \) band, respectively.

unambiguously detected. We show in Figure 6 the resulting CCF components for the Be star and companion from the tomographic reconstruction using a model template with \( T_{\text{eff}} = 17 \, \text{kK} \). We detect a faint CCF peak for the companion that reaches a level about five times higher than the background standard deviation of the CCF (measured over the velocity range 600 km s\(^{-1}\) < \( |V_c| < 1000\) km s\(^{-1}\)). This peak appears narrow, suggesting a low \( v \, \sin i \), as found for other stripped companions (Wang et al. 2021), and it appears at a similar systemic velocity as measured for the Be star CCF component (\(-11.0 \pm 1.1 \) and \(-14.8 \pm 1.2 \) km s\(^{-1}\) for the companion and Be star, respectively). The ratio of peak-to-background standard deviation for the companion CCF attains a maximum at \( T_{\text{eff}} = 16.7 \pm 2.0 \) kK. We made a simulation of model binary spectra for the Be star \( (T_{\text{eff}} = 14 \, \text{kK}, \log g = 3.5, V \sin i = 200 \) km s\(^{-1}\)) plus the companion for the same set of observed Doppler shifts and specific values of the monochromatic flux ratio \( f_{\text{phot,FUV}} \). We used the simulations to compare the ratio of CCF peaks in the models to those observed, and a match is obtained for a flux ratio of \( f_{\text{phot,FUV}} = 2.3% \pm 0.5% \) at 1500 Å. This agrees with expectations based upon model atmospheres and the \( H \)-band stellar flux ratio obtained from interferometry (while neglecting a possible small contribution by the disk), which for the same \( T_{\text{eff}} \) predict an sdB radius of \( R_{\text{comp}} = 0.69 \pm 0.07 \, R_\odot \) and flux ratios of \( f_{\text{phot,FUV}} = 3.3% \pm 0.5% \) and \( f_{\text{phot,K}} = 1.6% \pm 0.5% \). Including a possible flux contribution by the almost-dissipated disk decreases the values of the predicted flux ratios, leading to a still improved agreement. The expected flux ratio in the visible \( (\lambda = 5000 \) Å) is \( \sim 1.8% \), so it may be possible to detect the companion spectroscopically in the visible with renewed efforts.

5. Discussion, Conclusions, and Outlook

Our state-of-the-art \( H \)- and \( K \)-band interferometry has directly detected the companion to the classical Be star \( \kappa \) Dra. Together with the orbital RV amplitude of the Be primary measured in optical spectra and the parallax from Hipparcos and Gaia, these results enabled us to derive a full 3D orbital solution (Table 6) and the absolute masses and other fundamental parameters of both components (Table 7). Using these results and the measured near-IR flux ratios between the components, we excluded a late-type MS star or a WD nature of the companion, while an evolved late-type star is ruled out by a lack of corresponding IR excess. In a targeted search, guided by the derived orbital solution and the previous nondetection in the FUV of an sdO companion, we successfully detected a stripped-down sdB companion, making \( \kappa \) Dra the first firm case of a Be+sdB system, where the sdB companion has a substantially lower temperature than all of the
known sdO companions (found around hotter Be star primaries).

Presently, the B6 primary star of κ Dra is the lowest-mass Be star with a directly detected companion. The sdB nature of the companion is in contrast with early-type Be binaries with detected stellar companions, among which sdO companions dominate (maybe even exclusively). This contrast may be due to a bias in the observational analyses of FUV spectra, in which the standard cross-correlation technique was optimized for the detection of sdO secondaries, which is the reason why the sdB companion to κ Dra had not been previously detected (Wang et al. 2017). The example of κ Dra suggests that the search for hot low-mass companions in FUV spectra should be extended to the sdB domain, especially for cooler Be stars. In combination with optical long-baseline interferometry, this can clarify whether or not there is any correlation between the mass of the Be primaries and the nature of those secondaries that are not NSs.

A dependence of the type of the companion on the mass of the Be star is clear for NS companions, which are not found around mid- or late-type Be stars (Section 1). This is explained by the need for a massive progenitor of the secondary so that it could explode as a supernova. Figure 7 shows an H-R diagram with the component parameters of the known (early) Be+sdO systems complemented by the B6e+sdB system κ Dra and the B8n+pre-WD system Regulus. It appears plausible that there might be a hidden population of sdB or (pre-)WD companions around cooler Be stars so that the nature of the companion indeed correlates with the mass of the primary Be star. The discovery of a stripped sdB companion should be a useful reference for binary stellar evolution models, as, for instance, the evolutionary grid of Götberg et al. (2018) does not predict stripped companions with $T_{\text{eff}} < 20$ kK, and it expects a stripped star with a mass similar to the sdB companion of κ Dra to have $T_{\text{eff}} = 25.6$ kK. However, it is possible that the companion to κ Dra has already entered the WD cooling sequence.

The evidence that Be stars with subdwarf (and NS) companions owe their rapid rotation to mass and angular-momentum transfer in a close binary seems compelling. However, for the characterization of the population of classical Be stars at the time of their formation, a larger number of physical parameter sets and any nondetections of stellar companions of present-day Be stars are needed. A critical bottleneck is the RV measurements. For the RVs of the Be primaries, the large mass ratio and the strongly rotationally broadened photospheric lines require good data and careful analysis, as the case of κ Dra has confirmed. Because of the large brightness difference, RV determinations of subdwarfs orbiting Be stars are difficult (Wang et al. 2021). The case of κ Dra (in which statistical errors of ~13% and ~9% have been obtained for the masses of the primary and secondary, respectively) has illustrated how precise parallaxes can be used as a substitute for missing RVs of one of the two stars.

For low-mass companions, the large flux ratio at the operating wavelengths of Hipparcos and Gaia becomes an advantage because the effect of the orbital motions on the astrometric solution is less detrimental. But very high fluxes saturate the detectors and, contrary to first intuition, do not automatically promise larger parallaxes. According to the BeSS database, the two dozen Be stars that are visually brighter than κ Dra are mostly of earlier spectral type, and their higher intrinsic brightness implies distances that can actually be larger. This double disadvantage is alleviated for stars similar to κ Dra in both spectral type and apparent magnitude, of which well over a dozen exist. Studies of these lower-mass Be stars can complement the more massive Be star population with detected sdO stars. A more representative sample of Be stars and subdwarf companions will deliver important input to models for the evolution of close binaries. Any nondetections may

### Table 7

| Component | $M$ ($M_\odot$) | $T_{\text{eff}}$ (K) | $R$ ($R_\odot$) | $L$ ($L_\odot$) | $\nu$ sin $i$ (km s$^{-1}$) | $M_V$ (mag) |
|-----------|----------------|----------------------|----------------|----------------|----------------|-------------|
| Be        | 3.65 ± 0.48    | 13.982 ± 392$^a$     | 5.85 ± 0.18$^b$ | 1178 ± 151     | 200 ± 12$^a$   | −1.95 ± 0.40$^b$ |
| sdB       | 0.426 ± 0.043  | 16.70 ± 2000         | 0.69 ± 0.07    | 33 ± 17        | 35 ± 10        | 2.4 ± 0.4   |

Notes.

$^a$ Frémat et al. (2005).

$^b$ Touhami et al. (2013) + Gaia DR3 parallax.
have a bearing on the fraction of Be stars, if any, that do not form through mass transfer in a binary.

Object \( \kappa \) Dra is only the fifth Be binary for which dynamical masses have been determined (Section 1). Of these, the Be stars in \( \phi \) Per (Mourard et al. 2015) and V2119 Cyg (Klement et al. 2022) have masses that are in agreement with their spectral types. The Be star in the triple system \( \nu \) Gem (for this star, a compact companion is not known) is of the same spectral type as \( \kappa \) Dra, but at 3.33 \( \pm 0.10 \) \( M_\odot \) (Klement et al. 2021), it is even slightly more undermassive than \( \kappa \) Dra. Something similar probably holds for 60 Cyg, in which the Be star has a dynamical mass of 7.7 \( \pm 1.2 \) \( M_\odot \) (Klement, unpublished update of Klement et al. 2022, based on new observations), whereas its spectral type, B1Ve (Slettebak 1982), suggests 13.5 and 11.98 \( \pm 1.7 \) \( M_\odot \) for the calibrations of Harmanec (1988) and Hohle et al. (2010), respectively. At the current low level of knowledge and understanding, undermassive appears crudely equivalent to overluminous. This is not implausible for mass gainers that also gained thermal energy through the accretion and may experience enhanced mixing if the added gas has a higher molecular weight. Furthermore, more advanced evolution may contribute to the overluminosity. To assess the possibility of systematic differences between Be and non-Be stars in their fundamental parameters will be an important objective of future interferometry of Be stars. As this study of \( \kappa \) Dra has shown, the availability of RVs with matching quality can be decisive.

Of high interest also are the parameters that may trace the evolution of \( \kappa \) Dra as a system, beyond that of its individual components. The vanishingly small eccentricity is in agreement with orbital circularization due to tidal forces during the mass transfer. The disk appears to be coplanar with the orbit, as would be expected, but high-resolution spectrophotometry across prominent emission lines would be needed to deduce whether the angular-momentum vectors of the disk and the orbit are parallel or antiparallel. In the latter case, one might wonder whether an initial third body, for which there is no evidence, could link such a peculiarity and the relatively high space velocity (see Section 2.1).

This work is based upon observations obtained with the Georgia State University Center for High Angular Resolution Astronomy Array at Mount Wilson Observatory. The CHARA Array is supported by the National Science Foundation under grant Nos. AST-1636624 and AST-2034336. Institutional support has been provided to the GSU College of Arts and Sciences and the GSU Office of the Vice President for Research and Economic Development. MIRC-X received funding from the European Research Council (ERC) under the European Union’s Horizon 2020 research and innovation program (grant No. 639889), and N.A., C.L.D., and S.K. acknowledge funding from the same grant. Based on INES data from the IUE satellite. This research has made use of the SIMBAD database, operated at CDS, Strasbourg, France. This work has made use of the BeSS database, operated at LESIA, Observatoire de Meudon, France: http://basebe.obspm.fr. This research has made use of NASA’s Astrophysics Data System. This work has made use of data from the European Space Agency (ESA) mission Gaia (https://www.cosmos.esa.int/gaia), processed by the Gaia Data Processing and Analysis Consortium (DPAC; https://www.cosmos.esa.int/web/gaia/dpac/consortium). Funding for the DPAC has been provided by national institutions, in particular the institutions participating in the Gaia Multilateral Agreement. R.K. is grateful for a postdoctoral associateship funded by the Provost’s Office of Georgia State University. The research of R.K. is also supported by the National Science Foundation under grant No. AST-1908026. This research has made use of the Jean-Marie Mariotti Center Aspro, OIPFits Explorer, and SearchCal services (available at http://www.jmmc.fr/aspro and http://www.jmmc.fr/searchcal). R.K. expresses sincere thanks to the CHARA science staff, namely, Matthew D. Anderson, Theo ten Brummelaar, Christopher Farrington, Rainer Koehler, Robert Ligon, Olli Majoinen, Nicholas Scott, Judit Sturmann, Laszlo Sturmann, Nils Turner, and Norman Vargas, for making the observations used in this study. A.C.C. acknowledges support from CNPq (grant 311446/2019-1) and FAPESP (grants 2018/04055-8 and 2019/13354-1). S.K. acknowledges support from an ERC Consolidator Grant (grant agreement ID 101003096) and STFC Consolidated Grant (ST/V000721/1). J.D.M. acknowledges funding for the development of MIRC-X (NASA-XRP NNX16AD43G, NSF-AST 1909165) and MYSTIC (NSF-ATI 1506540, NSF-AST 1909165). P.T. acknowledges CAPES funding under grant 88887.604774/2021-00.

Facilities: Akari, CFHT, CHARA, Gaia, Hipparcos, IRAS, IUE, OHP:1.93 m, OO2, TBL, WISE.

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### References

Anugu, N., Le Bouquin, J.-B., Monnier, J. D., et al. 2020, AJ, 160, 158
Baade, D., Pigulski, A., Rivinius, T., et al. 2018a, A&A, 620, A145
Baade, D., Rivinius, T., Pigulski, A., et al. 2018b, in 3rd BRITE Science Conf. 8, ed. G. A. Wade et al. (Warsaw: PAS), 69
Baranne, A., Queloz, D., Mayor, M., et al. 1996, A&AS, 119, 373
Batten, A. H. 1973, Binary and Multiple Systems of Stars (New York: Pergamon Press)
Baudrand, J., & Bohm, T. 1992, A&A, 259, 711
Beichman, C. A., Neugebauer, G., Habing, H. J., Clegg, P., & Chester, T. J. 1988, Infrared Astronomical Satellite (IRAS) Catalogs and Atlases. Volume 1: Explanatory Supplement (Washington, DC: NASA), 1
