High performance cryogen-free microkelvin platform

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Improved accessibility to the microkelvin temperature regime is important for future research in quantum materials; for quantum information science; and for applications of quantum sensors. Here we report the design and performance of a microkelvin platform based on a nuclear demagnetization stage, engineered and well optimized for operation on a standard cryogen-free dilution refrigerator. PrNi5 is used as the dominant refrigerant. The platform provides a large area for mounting experiments in an ultralow temperature, low electromagnetic noise environment. The performance is characterized using current sensing noise thermometry. Temperatures as low as 395 µK have been reached, and a protocol has been established in which it is possible to operate experiments below 1 mK for 95% of the time, providing an efficient cryogen-free microkelvin environment for a wide range of science applications.

I. BACKGROUND

Advances in cryogen-free dilution refrigeration [1, 2] have played a crucial role in the development of superconducting quantum technology for computing and sensing. The microkelvin temperature regime represents a strategically important frontier for quantum information science. Cryogen-free technology is essential to promote the accessibility of this regime and to ensure sustainability, beyond specialist infrastructures such as the European Microkelvin Platform [3]. Cooling into this regime is achieved by adiabatic nuclear demagnetization [4]. The nuclear spins of a suitable material are polarized in an external magnetic field and cooled to dilution refrigerator temperatures. After thermally isolating the material, the external field is then reduced. Under approaching isentropic conditions, in the absence of interactions, \( T_f = T_i B_f / B_i \), where \( T_f, B_f \) refer to the final and initial temperature and magnetic field.

The range of quantum materials and quantum sensors of interest for quantum information science is extremely diverse. Access to lower temperatures will yield fundamental insights into two-level fluctuators in superconducting qubits [5], which are a barrier to fault-tolerant quantum computing [7, 8]. Further cooling of two dimensional electron gases [9], will promote understanding of aspects of the fractional quantum Hall effect [10] and drive the development of semiconductor devices, including spintronic devices [11, 12]. There is an ongoing search for a crystalline topological superconductor [13,18] and YbRh2Si2 [19] is a candidate material that requires temperatures below a few mK. When cooling below 2.5 mK \(^3\)He provides a benchmark for topological superconductivity, displaying a wealth of phenomena in the surface and edge states that arise from bulk-surface correspondence [20–23]. Strongly correlated electron systems exhibit quantum criticality [24,26], which is essentially a \( T = 0 \) phenomenon. An exciting direction is the extension of studies of quantum criticality to lower temperature, for example to understand the role of nuclear magnetism, particularly in systems with strong hyperfine interactions [27,30]. Cooling to below 1 mK allows access to magnetic field-to-temperature ratios, \( B/T \), unachievable elsewhere. High \( B/T \) ratios are of particular interest in heavy fermion systems and also to investigate hyperfine effects. Finally microkelvin platforms will be of increasing importance for hosting quantum sensors for fundamental physics, such as dark matter searches and quantum simulators. These may require locating in underground facilities, where cryogen-free operation is optimal.

Significant effort has been devoted to on-chip cooling technologies [31,32]. Two successful approaches to reaching microkelvin temperatures have been either by parallel nuclear demagnetization of each lead connected to a sample [33,34] or by the incorporation of nuclear refrigeration elements directly on-chip, where the device is itself a thermometer (a Coulomb blockade thermometer), which directly measured the electron temperature [35,36].

Our approach is to treat the cooling of the microkelvin platform and the thermalization of the device/sample to this platform separately. The merit of this approach is its flexibility and applicability to a wide range of materials and devices. On traditional “wet-cryostats” we have demonstrated: cooling of a two dimensional electron gas below 1 mK in a \(^3\)He immersion cell [37], thermodynamic and transport measurements on a heavy fermion superconductor YbRh2Si2 down to 200 µK [38]; and an ac susceptibility study of superconductivity and antiferroquadrupole order in PrOs4Sb12 [39] down to 1 mK, reaching a \( B/T \) in excess of 6000 T/K. In combination with cryogen-free operation this opens a wide landscape for research on quantum materials into the microkelvin...
II. INTRODUCTION

A proof-of-principle cryogen-free nuclear demagnetization platform [40] was based upon a PrNi$_5$ nuclear stage, that had been originally constructed for a traditional “wet-system” [41]. This demonstrated that the vibrations inherent in a pulse-tube cooled cryostat [42] are not incompatible with nuclear demagnetization. Cryogen-free systems with copper nuclear demagnetization stages have been developed reaching temperatures below 100 µK [34, 43, 44]. Designs of continuous cryogen-free nuclear demagnetization systems have been proposed [45, 46] but have yet to have demonstrated their performance.

The focus of this paper is a cryogen-free microkelvin platform capable of achieving temperatures below 500 µK with a hold time below 1 mK suitable for the applications discussed previously. A rapid thermal turnaround time dramatically enhances the efficiency of an experiment, with a greater fraction of time being spent in the temperature range of interest. A key figure of merit is the thermal “duty cycle”, which we define as the percentage of the total time of the single-shot cooling cycle spent below 1 mK. For our design the best value achieved so far is 95%, a dramatic improvement over the previous published results for cryogen-free systems, ranging from 50% down to < 10% [40, 43, 44].

To achieve this result we combined the favorable properties of the Van Vleck paramagnetic material PrNi$_5$, which has previously been used in traditional “wet-cryostats” [4, 47–51], with a well designed thermal link, heat switch and system to minimize the relative motion between the demagnetization magnet and nuclear stage.

Essential to the characterization of the performance of the system is reliable thermometry. We adopted current sensing noise thermometry (CSNT) [52, 53], which can be used over the full temperature range.

III. DESIGN DETAILS

The design principle was for a system that would be compatible with a minimally modified cryogen-free dilution refrigerator, boosting the lowest temperatures that could be reached to below 500 µK (in this case an Oxford Instruments Triton 200 [54]). The system was equipped with a 6 T superconducting magnet. Field compensation results in less than 10 mT in the ultralow temperature (ULT) experimental region, when the magnet is at the full field. We adopted a modular design in which the thermal links interconnecting the main components of the platform used demountable cone joints [55].

A schematic of the system is shown in Fig. 1. All of the copper used in the construction was commercial OFE-OK copper [56]. Through heat treatment the residual resistivity ratio (RRR) of the copper could be increased up to 3000. The mixing chamber (MC) plate, the heat switch (HS) plate, and the ULT plate were gold-plated to prevent oxidization of the surfaces [57]. Each plate was equipped with a 4-wire resistive heater for characterization. Simplicity and reproducibility of construction, and the avoidance of hazardous materials and toxic chemicals in the construction process were also design criteria.

The original cryostat MC plate was replaced by a design to meet the requirement for an RF-tight space for the microkelvin platform. The MC shield and plate enclose a large volume, creating an electrically quiet environment for measurements while reducing the heat leak to the ULT region. The HS magnet is mounted on the MC plate, outside of the RF shield. A CSNT (sensor resistance 300 mΩ) was mounted on the MC plate.

The experimental volume contains a relatively large area ULT plate, of diameter 240 mm, with a RRR of 265. The ULT plate is equipped with multiple mount-
ing points for experiments, consisting of 14 cone joints, 3 of which have line-of-sight access to the room temperature ports on the top of the cryostat. The ULT plate is suspended from the MC plate via alumina tubes. The thermal pathway to the MC plate is via a flexible copper link (annealed to achieve a RRR of 3000), the HS plate and the robust indium heat switch. The HS plate is suspended from the MC plate using Vespel rods. A CSNT (sensor resistance 2 mΩ) was mounted on the ULT plate and was used to characterize the performance of the demagnetization process.

The nuclear demagnetization stage was constructed out of polycrystalline PrNi\(_5\) of total mass 94.5 gm (0.22 mole), supplied in the form of irregular rods, soldered using indium to a rigid copper support structure. The copper support structure (RRR of 1660) is attached to the ULT plate by copper rods with cone joints at each end. While all of the construction materials contribute to nuclear cooling, the dominant contribution arises from the PrNi\(_5\). Hyperfine enhancement boosts the field seen by the \(^{141}\)Pr nuclei by a factor 11.2 above the externally applied field \(\mu_0 H\). In 6 T a significant entropy reduction (> 80%) of the PrNi\(_5\) can be achieved in the modest temperature range, 10 - 20 mK.

Praseodymium’s small Korringa constant \(\kappa\), results in a negligible thermal resistance between the electrons and the nuclear spin system (\(\kappa_{\text{Pr}} \sim 3 \mu\)Ks \(\mu_0 H\) compared to \(\kappa_{\text{Cu}} = 1.2 \mu\)Ks for copper \(\mu_0 H\)). The thermal conductivity of polycrystalline PrNi\(_5\) is poor, comparable to brass. The PrNi\(_5\) rods had a RRR that varied from 7 to 30. It is therefore critical to optimize the heat transfer between the copper support structure and the PrNi\(_5\). This was achieved using indium as a solder \(\mu_0 H\). Cadmium has traditionally been used for this purpose \(\mu_0 H\), but has higher toxicity, zinc has recently been proposed \(\mu_0 H\) as an alternative material. Although indium limits the final field to be in excess of 28 mT, the superconducting critical field of indium, it did not compromise the achievement of the performance objectives.

To achieve a short precooling time, the thermal link between the MC plate and the nuclear stage was designed to be dominant relative to the cooling power of the MC. For comparison at the end of the precool shown in figure 2 the cooling power of the dilution refrigerator was \(Q = 5 \mu\text{W}\), resulting in \(Q/T^2 \sim 12.2 \text{mW/K}^2\), less than half of the value \(L/2R = 27 \text{mW/K}^2\) due to the thermal link, where \(L\) is the Lorenz number \(\mu_0 H\) and \(R \sim 450 \text{n} \Omega\) is the total resistance between the PrNi\(_5\) and the MC. Figure 1 shows this thermal pathway in two sections, Path A, between the MC and ULT plate, and Path B, between the ULT plate and the Pr nuclear spin bath. The measured thermal resistance of Path A, with the heat switch in its normal state, corresponds, via the Weidemann-Franz law \(\mu_0 H\), to an electrical resistance of 300 nΩ. The superconducting heat switch assembly including cone joints contributes 170 nΩ to this value. The thermal conductivity of the open switch, measured at 100 mK is \(3\times10^{-5} \text{Wcm}^{-1}\text{K}^{-1}\), equivalent to that achieved in aluminum heat switches \(\mu_0 H\). The thermal resistance of Path B was measured directly, by applying heat to the ULT plate, and corresponded to an electrical resistance of 150 nΩ.

Key to the cooling performance achieved is the immunity to mechanical vibrations. It is most important to limit relative motion of the nuclear stage and the 6 T magnet. This is achieved by three similar “bicycle-wheel” spacers: between stage and MC shield; between MC shield and still shield; and between the still shield and main magnet (see Fig.1 and Fig.5 inset).

IV. PERFORMANCE

To illustrate the duty cycle we show in Fig.2 a process in which the system starts in a low field at 9 mK, it is magnetized to 6 T, followed by a rapid pre-cool period of about 2 hours. We refer to this as a “lunchtime” precool. After opening the superconducting heat switch, a demagnetization to a final field of 30 mT at a constant rate of 1.75 T/hour gives a final temperature around 500 mK. The heat leak due to eddy currents was measured to be 30 nW in the field interval 5.6 T to 4.5 T. The platform remains below 1 mK for almost 6 days. With longer precool time (15 hours, referred to as an “overnight” precool), the starting temperature of the demagnetization is typically 10 mK and with a staggered demagnetization rate over a period of 7.5 hours a temperature of 395 mK was achieved. Eddy current heating in the copper structure, arising from vibrations while pre-cooling in the high magnetic field and sweeping of the field during demagnetization, is tolerable despite its geometry and high RRR. Here we exploit the high magneto-resistance of copper \(\mu_0 H\); with a RRR = 1660 the electrical resistance increases by a factor of over 20 in 6 T.

To quantify the heat leak and its field dependence the total heat capacity of the nuclear stage was measured using the CSNT and a heater on the ULT plate. We exploit the achievable precision in short measurement times, \(t_m\), using two-stage SQUID detection \(\mu_0 H\). The noise floor of these devices allow the sensor resistor to be from a few mΩ to a few hundred mΩ and still have a reasonable noise temperature (in the range 5 mK to 100 mK). The 2 mΩ sensor of the CSNT delivers 1% precision in \(t_m=10\) s \(\mu_0 H\).

A typical heat pulse is shown in Fig.3. The total stage heat capacity measured in this way for various magnetic fields is shown in Fig.4. The residual heat leak in different magnetic fields is determined by simply observing the warm up rate, Fig.5. We note that with this level of heat leak in low fields, and the experimentally determined thermal resistance between the ULT plate and the PrNi\(_5\), we can be confident that the CSNT is in good equilibrium with the stage. Thermalization of the CSNT to the ULT plate relies on filtering the leads between the SQUID and the sensor resistor \(\mu_0 H\).

The 4 nW field independent heat leak at low fields
FIG. 2. a) Preparation time for a “lunchtime” precool; the external magnetic field is ramped up to 6 T (green); the magnet is persisted and the nuclear stage is allowed to pre-cool (blue); the heat switch is opened and the nuclear stage is demagnetized to 30 mT (pink). b) Temperature of the ULT plate CSNT as a function of time following the demagnetization, showing a hold-time of 140 hours below 1 mK.

Fig. 5 was subsequently reduced to 2 nW, by improvements in electrical and mechanical grounding of room temperature services. The warm-up data in Fig. 2 was determined under these conditions, and we estimate that the “overnight” pre-cool will result in two weeks below 1 mK with such a low heat leak.

V. CONCLUSION

We have demonstrated the performance of a microkelvin platform, that is modular, robust, and tolerant to mechanical vibrations. The platform can rapidly reach temperatures as low as 395 µK. The holdtime below 1 mK represents an excellent duty cycle of 95%.

The platform provides a large electrically quiet experimental microkelvin volume, capable of hosting multiple experiments, including those requiring line-of-sight access to room temperature.

The modularity of the design ensures compatibility for upgrading existing cryogen-free dilution refrigerators, offering the opportunity for an order of magnitude decrease in their base temperature. To promote future sustainability and reduce the environmental impact the manufacturing processes were designed to minimize the use of toxic and hazardous materials. The technological importance of PrNi$_5$ as a working material motivates the growth of samples of improved quality.

This work moves us from a proof-of-principle to a prototype system, with very limited demands on the surrounding infrastructure. The internal levels of vibration isolation achieved were sufficient to produce a low heat leak to the demagnetization stage, without massive support structures and optical-table quality air-mounts. As such this is a significant step towards the accessibility of microkelvin temperatures, opening up a frontier in quantum information science and quantum material research to the widest possible community.

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FIG. 4. Total heat capacity of the nuclear stage as a function of temperature and applied magnetic field, with PrNi$_5$ providing the dominant contribution.

FIG. 5. The heat leak to the nuclear demagnetization stage as a function of external magnetic field, extracted from warming data. Subsequent improvements resulted in a 30 mT heat leak of 2 nW, which is the heat leak under which the warming data shown in Fig.2 was obtained. Inset: “Bicycle-wheel” components connecting the still shield to the magnet.
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