Theoretical study of core-loss electron energy-loss spectroscopy at graphene nanoribbon edges

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Abstract

A systematic study of simulated atomic-resolution electronic energy-loss spectroscopy (EELS) for different graphene nanoribbons (GNRs) is presented. The results of ab initio studies of carbon 1s core-loss EELS on GNRs with different ribbon edge structures and different hydrogen terminations show that theoretical core-loss EELS can distinguish key structural features at the atomic scale. In addition, the combination of polarized core-loss EELS with symmetry resolved electronic partial density of states calculations can be used to identify the origins of all the primary features in the spectra. For example, the nature of the GNR edge structure (armchair, zigzag, etc) can be identified, along with the degree of hydrogenation. Hence it is possible to use the combination of ab initio calculations with high resolution, high energy transmission core-loss EELS experiments to determine the local atomic arrangement and chemical bonding states (i.e. a structural fingerprint) in GNRs, which is essential for future practical applications of graphene.

Keywords: graphene, nanoribbon, EELS, DFT

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(Some figures may appear in colour only in the online journal)

1. Introduction

Graphene is an extraordinary material, comprising a single layer of carbon atoms, with remarkable properties, as noted in many recent review articles e.g. [1–4]. To fully utilize its electronic properties in device applications, there is a need to tailor the properties as the perfect infinite sheet is a semi-metal, and so some form of band-gap engineering is required. One very promising approach is to cut the sheet up into a graphene nanoribbon (GNR), which then opens up a width-dependent electronic energy band-gap [5]. The properties of GNRs are known to be sensitive to local atomic configurations [6, 7] and so elemental identification and electronic state analysis at the atomic scale is becoming increasingly important. So far, the atomic configurations at graphene nanoribbon edges have been investigated by transmission electron microscopy [8, 9] and scanning probe techniques [10] but the electronic properties of the edge states has not yet been determined with atomic resolution.

Recently, there have been significant developments in energy-loss near-edge fine structure (ELNES) measurements, with a state-of-the art atomic resolution study of carbon 1s core-loss ELNES for different graphene nanoribbon edges reported by Suenaga and Koshino [11]. Such measurements required detailed theoretical modelling for a full understanding, and so in this work, a detailed study of the predicted ELNES spectra for various GNR edges and different hydrogen terminations is presented. This can then be
used as a fingerprint for the interpretation of experimental ELNES measurements. ELNES is an example of electron energy-loss spectroscopy (EELS)—hence all the comments here apply to the general EELS approach. However, it should be noted that in this work the focus is on high energy transmission EELS. If elastic scattering effects are properly taken into account, then EELS spectra taken in strong diffraction conditions (including those of the reflection EELS geometry) could also be taken into account, but that is beyond the scope of the current study. The carbon 1s core-losses can be easily distinguished from the low energy losses associated with both single particle and collective excitations of the valence electrons because they occur at different energies. Finally, in transmission EELS it is possible to perform the EELS measurements either in spatially or momentum-resolved modes wherein the momentum transfer wavevector $q$ is analogous to the polarization vector in x-ray absorption spectra. Using differential methods [12, 13], the effect of the orientation of the polarization vector on the EELS spectra can be studied with a highly localized probe, with nanometer resolution.

### Table 1. Summary of the edge formation energies.

| Structure     | Edge formation energy (eV) |
|---------------|---------------------------|
|               | This work | Koskinen *et al* [19] |
| ZGNR          | 3.469     | 3.22                   |
| Klein+H       | 2.928     |                        |
| ZZ57          | 2.574     | 2.36                   |
| AGNR          | 2.287     | 2.09                   |
| Klein+2H      | 1.166     |                        |
| Klein+3H      | 0.753     |                        |
| ZGNR+H        | 0.223     |                        |
| AGNR+H        | 0.050     |                        |
| ZGNR+2H       | −0.078    | +0.15                  |
| AGNR+2H       | −0.357    | +0.02                  |

*Note: Smaller values are more energetically favoured.*

### 2. Method

*Ab initio* calculations of the electronic structure of various GNRs were performed using the CASTEP [14, 15] plane-wave
density functional theory (DFT) [16] code. The local density approximation exchange-correlation functional [17] was used, as that gives excellent structures for graphene materials without needing any extra dispersion correction. The simulation of an isolated GNR was achieved by using the supercell approach, with rigorous tests to make sure that the calculated EELS spectra were fully converged w.r.t. parameters such as periodic distance (the core-hole has a finite range, and to simulate an isolated core-hole requires a sample size of at least 8 Å in-plane direction), and the vacuum gap (the higher energy orbitals can be quite diffuse and give rise to spurious features in the EELS spectra unless the inter-layer separation is at least 14 Å). Brillouin zone sampling was done using Monkhorst–Pack grids with a sample density of $\frac{1}{2\pi} \times 0.022 \text{Å}^{-1}$. See the supplementary information for more details (stacks.iop.org/JPhysCM/27/305301/mmedia).

A specially constructed double-projector norm-conserving pseudopotential was used, with a 1s core-hole on one atom, using the ‘on-the-fly’ methodology within CASTEP which is necessary for the core-states to be fully reconstructed in order to calculate the core-loss EELS spectra. The spectra plotted correspond to the modulus-squared of the dipole transition matrix elements,

$$I(E) = \sum_{\mathbf{k}} \omega_{\mathbf{k}} \sum_n \gamma(E - E_{n,\mathbf{k}}) \left| \langle \phi_d | \psi_{n,\mathbf{k}} \rangle \right|^2$$  \hspace{1cm} (1)

where the summation is over unoccupied states $n$ and Brillouin zone sample points $\mathbf{k}$ with weights $\omega_{\mathbf{k}}$, $\langle \phi_d | \psi_{n,\mathbf{k}} \rangle$ is the core state on the site of interest and $\psi_{n,\mathbf{k}}$ is a (single particle) conduction state. Finally, due to the limited number of sampling points, a Lorentz broadening function $\gamma(E - E_{n,\mathbf{k}})$ was incorporated into the Brillouin zone spectral integration. Full details on the pseudopotential core-loss EELS methodology are in [18]. Additional details on the calculations and data such as convergence with ribbon width are included in the supplemental material (stacks.iop.org/JPhysCM/27/305301/mmedia).

The structures considered were all electrically neutral, and so the following simple expression was sufficient to define the formation energy of the two edges of the graphene nanoribbon $E_{\text{edge}}$: Fig. 2. Atom-resolved core-loss EELS for each of the distinct sites in an unhydrogenated AGNR. (a) shows the labeling of each site and the coordinate system used. (b) shows the calculated core-loss EELS for a core-hole on the labelled carbon atom, and ‘total’ shows the effect of averaging the core-loss EELS across all sites. Four distinct peaks are visible, labelled P1 to P4—see text for a discussion.
\[ E_{\text{GNR}}^{\text{edge}} = \frac{E_{\text{total}}^{\text{GNR}} - N_c \mu_C - N_H \mu_H}{N_c^{\text{edge}}} \]  

where \( N_c \) is the total number of carbon atoms in the ribbon, \( N_c^{\text{edge}} \) is the number of carbon atoms at the two edges of the ribbon, \( N_H \) is the number of passivation hydrogen atoms added in total at both edges, \( E_{\text{total}}^{\text{GNR}} \) is the electronic total energy of the ribbon containing \( N_c + N_H \) atoms, \( \mu_C \) is the chemical potential of carbon and \( \mu_H \) is the chemical potential of hydrogen. The carbon atoms are assumed to come from a reservoir of...
core-loss + electron excitation spectroscopy - edge onset is at 0 eV. The general accuracy of this and which can be passivated with up to has a carbon atom with a single bond to the rest of the ribbon, which is the less commonly studied Klein edge [20], which why it was not discovered for a long time. between this and the reconstructed zz-57 structure, which is minimum and is metastable, and that there is an energy barrier that the unreconstructed ZGNR corresponds to a local energy of ZGNR in the absence of hydrogen. It should be noted heptagon. This has been shown [19] to be the more favoured hexagons at the zigzag edge reconstruct into a pentagon and a zigzag edge reconstruction (zz-57) - in which two adjoining morphs, the accuracy of DFT calculated EELS compared to experiments has also been demonstrated [22]. For each structure considered, the carbon 1s core-loss EELS spectrum was calculated up to 60 eV above the onset, and then normalized so that the integrated area from 0–60 eV was unity. By selecting different sites for the core-hole, it is possible to generate an atom-resolved core-loss EELS, which is the level of spatial resolution that is now becoming experimentally available. It is also possible to average the different site-resolved spectra, with appropriate weighting for the number of different equivalent sites, to generate a total spectrum representing a low-spatial resolution experiment, being the core-loss EELS for the total ribbon.

3. Results
3.1. Edge formation energies
There is a small variation in the edge formation energy with GNR width, with reasonable convergence for widths greater than 8 Å wide. The Klein-edge structure is unstable without any hydrogen passivation, with a reconstruction to a structure with two neighbouring edge carbon atoms bonding to make a 5-member ring. With hydrogen passivation, the Klein edge is a local energy minimum without a significant carbon reconstruction. Both AGNR and ZGNR are unable to accept +3H per edge carbon atom.

The edge formation energy for all the fully relaxed edge structures considered are included in table 1. This shows that for both ZGNR and AGNR the most stable edge has +2H per edge carbon atom, whilst the Klein edge is most stable when it has +3H per edge carbon atom. The large negative formation
energies for AGNR+2H shows that this edge is unequivocally thermodynamically stable and can spontaneously form. The small energies for AGNR+H and ZGNR+2H suggest that they are probably stable at room temperature, whilst the larger positive values for all the other edges suggest these edge are metastable, and may only be stable in vacuum or a very low hydrogen content environment. All of these structures have been seen experimentally [8, 10, 23].

3.2. Core-loss EELS spectra

3.2.1. Armchair graphene nano-ribbons. The calculated core-loss EELS for an unhydrogenated (unpassivated) AGNR is shown in figure 2. There are four distinct peaks visible, labelled P1 ... P4, whose identity can be determined by considering polarized core-loss EELS.

A perfect graphene sheet has higher symmetry than a GNR, and consequently if the applied electric field is polarized in the plane of the sheet (either X- or Y-direction here) then transitions into the anti-bonding states of \( \sigma^* \)-symmetry are allowed, but with Z-direction polarization then transitions into the anti-bonding states of \( \pi^* \)-symmetry are allowed. Hence by calculating the effect of different E-field polarizations on the core-loss EELS for a unhydrogenated AGNR as shown in figure 3, the origins of the main peaks can be determined. This shows that the dominant contribution to peak P1 is from the edge carbon atom (site 1) with the X-direction polarization and is consistent with the site-resolved core-loss EELS shown in figure 2. This is the only site in AGNR that has triple bonds, and therefore this peak can be assigned to the \( \pi^* \) state of the triple bonds in the X–Y plane. The P2 peak is present in the spectra of each atom and appears in the Z-direction and may therefore be assigned to the out-of-plane \( \pi^* \) state. Similarly, P3 and P4 mainly appear in the X- and Y-directions respectively, and can be assigned to in-plane \( \sigma^* \) states. In particular, P3 has a dominant contribution.

Figure 5. Atom-resolved core-loss EELS for each of the distinct sites in a mono-hydrogenated AGNR. (a) The labeling of each site and the coordinate system used. (b) The calculated core-loss EELS for a core-hole on the labelled carbon atom, and ‘total’ shows the effect of averaging the core-loss EELS across all sites. There is a qualitatively new peak visible in the core-loss EELS for site 1, that can therefore be attributed to the C–H bond that is found at this site and nowhere else in this AGNR.
from interchain bonds (i.e. bonds that are perpendicular to the GNR edge) and P4 from intrachain bonds (i.e. bonds that are parallel to the GNR edge).

In the same way, the effect of progressively increasing levels of hydrogenation (either 0, +1H or +2H per edge C atom) on the AGNR are shown in figure 4. The dominant $\sigma^*$ and $\pi^*$ peaks are easily visible, but there are clearly additional peaks that depend upon the degree of hydrogenation. This clearly shows the power of core-loss EELS to identify subtle structural differences. Note that hydrogen is usually

![Figure 6](image-url)
Figure 7. Comparison of atom-resolved core-loss EELS (top) and the projected electronic density of states (bottom) for the edge site in mono-hydrogenated AGNR. The PDOS makes a dominant contribution to the core-loss EELS spectrum and helps with the assignment of the symmetry of each peak.

Figure 8. Atom-resolved core-loss EELS for each of the distinct sites in a di-hydrogenated AGNR. (a) The labeling of each site and the coordinate system used. (b) The calculated core-loss EELS for a core-hole on the labelled carbon atom, and ‘total’ shows the effect of averaging the core-loss EELS across all sites. There are two qualitatively new peaks visible in the core-loss EELS for site 1, labelled A1 and A2. See text for a detailed discussion of these peaks.
very hard to detect in most forms of electron microscopy, and so this is an additional advantage to this approach—it is possible to identify the binding site and number of hydrogen atoms present.

A study of the sources of the difference in the core-loss EELS with hydrogenation is also possible by considering the site- and symmetry-resolved spectra. Figure 5 shows the atom-resolved core-loss EELS for a mono-hydrogenated (+1H) AGNR. Clearly there is a new peak that is visible when the core-hole is on the edge carbon atom, that is not present in the unhydrogenated AGNR, which can therefore be assigned to the C–H bond. The polarized E-field results shown in figure 6 confirms this suspicion—the new peak is visible in the X- and Y- directions but not Z, which proves that it is due to the C–H bond.

Finally, the projected electronic density of states (PDOS) for the edge carbon atom is shown in figure 7, along with the corresponding core-loss EELS. It is well known that the core-loss EELS depends upon the PDOS, but the symmetry resolution (projection onto angular momentum states) confirms the intuition that this extra peak is due to a transition to a \(\sigma^*\) state for the C–H bond. In general, the dipole selection

\[ \text{Figure 9. Effect of polarized E-field on the atom-resolved core-loss EELS for each of the distinct sites in a di-hydrogenated AGNR. Parts (a)–(c) show the effect of incident E-field that is polarized in the X-, Y- and Z- direction respectively. There are two new peaks that are associated with the two C–H bonds. Peak A1 is seen in the Z-direction, and peak A2 in the X- and Y-directions. The site labeling is the same as in figure 8.} \]
rule suggests that only \( p \)-states need to be considered, and for low energies (below 3 eV), figure 7 confirms that this is the dominant component of the core-loss EELS and hence only transitions to anti-bonding \( \pi^* \) states are possible. At higher energies, e.g. above 3 eV, there is evidence of \( s-p \) hybridization and transitions to \( \sigma^* \) states become possible. Note that the extra peak is seen in both \( X \)- and \( Y \)-directions and so is due to the \( \sigma^* \) state for the edge carbon atom, which has been red-shifted by about 4.7 eV compared to the other carbon atoms due to the longer C–C bond length for the edge atom.

Hence by combining symmetry-resolved PDOS and the polarized atom-resolved core-loss EELS it is possible to identify the detailed origins of the different peaks, which therefore underlines the usefulness of \( ab \ initio \) calculations for core-loss EELS studies.

A similar picture emerges from the study of the di-hydrogenated (+2H) AGNR. As can be seen in figure 8, the key difference is that there are now two C–H bonds per edge carbon which are out of the plane of the GNR. Comparison of the total spectrum with figure 4 shows that there are now two additional peaks (labelled A1 and A2) compared to the unhydrogenated AGNR. The site-resolved core-loss EELS shows that the key difference is in the spectrum associated with the edge carbon atom. The polarized core-loss EELS in figure 9 shows that A2 is associated with the \( Z \)-direction and A1 (which is actually a double peak) with the \( X \)- and \( Y \)-directions. Also, the low-energy \( \pi^* \) state is missing for site 1. This can be understood as the two C–H bonds are out of the plane of the AGNR which therefore suppresses the transition to the \( \pi^* \) state at this site. The A1 peak is a double peak, due to the two C–H bonds, but in the total spectrum the lower peak of
the doublet merges into the shoulder of the dominant $\sigma^*$ peak. Hence A1 is due to a transition to the $\sigma^*$ state for the C–H bond. The A2 peak is seen in both X- and Y- directions and so is due to the $\sigma^*$ state for the edge carbon atom, which has been red-shifted by about 2.9 eV compared to the other carbon atoms. This shift is due to the longer C–C bond length for the edge carbon due to the hydrogen saturation for this atom. The shift for the A2 peak is less than that for the A1 peak due to the level broadening caused by the two $\sigma^*$ states.

3.2.2. Zigzag graphene nano-ribbons. The site-resolved core-loss EELS for the unhydrogenated and unreconstructed ZGNR is shown in figure 10. As expected, the edge carbon atom is qualitatively different to the other sites. However,
whilst this structure is mechanically stable, it has a higher energy than the reconstructed $zz$-57 structure, and so it is the reconstructed structure that will later be studied in more detail. Note that the edge atom (site 1) has a very strong $\pi^*$ peak, due to the unoccupied edge state, which is the origin of the unpaired spin density and the AFM signature seen in

**Figure 12.** Effect of polarized $E$-field on the atom-resolved core-loss EELS for each of the distinct sites in a reconstructed $zz$-57 GNR. Parts (a)–(c) show the effect of incident $E$-field that is polarized in the $X$, $Y$ and $Z$ direction respectively. The site labeling is the same as in figure 11.
Figure 13. Effect of hydrogenation on the total core-loss EELS for a ZGNR.

Figure 14. Atom-resolved core-loss EELS for each of the distinct sites in a mono-hydrogenated ZGNR. (a) The labeling of each site and the coordinate system used. (b) The calculated core-loss EELS for a core-hole on the labelled carbon atom, and ‘total’ shows the effect of averaging the core-loss EELS across all sites. There is a qualitatively new peak visible in the total core-loss EELS that is labelled M. See text for more discussion.
This state is rapidly suppressed by reconstruction or hydrogenation (see below) which explains why AFM is not routinely observed in GNRs.

The site-resolved core-loss EELS for the reconstructed \( zz \)-57 structure (which is energetically more stable than the unhydrogenated and unreconstructed ZGNR structure in figure 10) is shown in figure 11. This structure has considerably lower symmetry than the simpler unreconstructed one, and consequently there are many more distinct sites to consider. The total core-loss EELS has four distinct peaks, labelled S1 ... S4 to be considered. Once again, consideration of the site-resolved spectra, in combination with the polarized...
Figure 16. Comparison of atom-resolved core-loss EELS (top) and the projected electronic density of states (bottom) for the edge site in mono-hydrogenated ZGNR. The PDOS makes a dominant contribution to the core-loss EELS spectrum and helps with the assignment of the symmetry of each peak.

Figure 17. Atom-resolved core-loss EELS for each of the distinct sites in a di-hydrogenated ZGNR. (a) The labeling of each site and the coordinate system used. (b) The calculated core-loss EELS for a core-hole on the labelled carbon atom, and 'total' shows the effect of averaging the core-loss EELS across all sites. There are two new peak visible in the core-loss EELS for site 1 that are labelled as D1 and D2. See text for detailed discussion.
core-loss EELS in figure 12, enables the peaks to be identified. Peak S1 is clearly the transition to the anti-bonding $\pi^*$ state of the triple bonds of the reconstructed edge atoms as it is very strong in the X-direction. Peak S2 is found in the Z-direction for all the core-hole sites and so corresponds to a $\sigma^*$ peak. Peak S3 is strong in the X-direction, whilst S4 is strong in the Y-direction (particularly for the inner carbon atoms 4–7) and so both can be assigned to $\sigma^*$ states.

The effect of hydrogenation on the ZGNR can be seen in figure 13. As with the AGNRs, there are distinct new features that can be seen upon the addition of hydrogen to the edge atoms. Note that the ‘non-passivation’ spectrum is that for the
unreconstructed ZGNR—this is so that the effect of hydrogen on the spectrum is clearer, as there is only a small change in the carbon atom positions upon hydrogenation. The reconstructed zz-57 GNR is more stable, but is unable to accept any hydrogen at all as there are no unpaired electrons at the edge sites. Hence whilst the zz-57 GNR structure is more stable than unreconstructed ZGNR in the absence of hydrogen, it can be seen from the results in table 1 that the situation is reversed in the presence of hydrogen.

A detailed study of the changes in the core-loss EELS upon hydrogen passivation can also be performed for ZGNR structures. The effect of mono-hydrogenation can be seen in figure 14 which clearly shows an additional peak (labelled M) that can be seen in the total core-loss EELS. On this occasion, it is not so obvious which site makes the dominant contribution to this peak, although there is a clear reduction in the low-energy $\pi^*$ peak due to the elimination of the unoccupied edge state. Close examination of the polarized core-loss EELS in figure 15 and the corresponding PDOS plot in figure 16 show that it is dominated by an $X$-direction component from site 1, and from a $Z$-direction component from all sites. Hence this peak cannot be attributed to a pure $\sigma^*(C-H)$ peak (unlike the corresponding situation in AGNRs) but also contains a contribution from $\pi^*$ state for all carbon atoms in the ribbon. This is confirmed by the PDOS plot showing strong contribution from both $s$- and $p$-states around 5 eV.

A similar picture is seen for the fully (di-)hydrogenated ZGNRs. As shown in figure 17, there are now two new peaks, labelled D1 and D2, that are not present in the unhydrogenated ZGNR, and associated with the edge carbon atom (site 1). Consideration of the site-resolved polarized core-loss EELS spectra in figure 18 suggests that whilst D2 seems to be a pure $\pi^*$ peak as it only appears in the $Z$-direction, the situation is more complex for the D1 peak. D1 is dominated by a $\sigma^*(C-H)$ peak (site 1, $X$-direction) but there is also a small component from the other carbon sites ($Z$-direction). This implies that there is some hybridization between the $\sigma^*(C-H)$ state and a $\pi^*$ state, which is therefore the origin of the energy difference between D1 and D2.

3.2.3. Klein-edge graphene nano-ribbons. The final GNR to consider is the Klein edge structure. This structure is less commonly studied than AGNR and ZGNR, but as shown in

![Figure 19. Atom-resolved core-loss EELS for each of the distinct sites in a di-hydrogenated Klein-edge GNR. (a) The labeling of each site and the coordinate system used. (b) The calculated core-loss EELS for a core-hole on the labelled carbon atom, and ‘total’ shows the effect of averaging the core-loss EELS across all sites. There are two new peaks visible in the core-loss EELS for site 1, that are labelled K1 and K2. See text for a detailed discussion.](image-url)
table 1, it can be energetically competitive with both AGNR and ZGNR structures. It can be considered as the addition of an extra carbon atom to a ZGNR edge, and as such has three unpaired electrons and hence is very reactive. The mono- and di-hydrogenated structures are qualitatively similar to the previous hydrogenated structures reported above, so only the most stable state, the tri-hydrogenated (3H) one, is reported here. The site-resolved and total core-loss EELS are shown in

![Figure 20](image-url)  
**Figure 20.** Effect of polarized $E$-field on the atom-resolved core-loss EELS for each of the distinct sites in a mono-hydrogenated ZGNR. Parts (a)–(c) show the effect of incident $E$-field that is polarized in the $X$-, $Y$- and $Z$- direction respectively. Two qualitatively new peaks are seen at site 1.
figure 19 and the corresponding polarized core-loss EELS in figure 20. Two qualitatively new peaks can be seen, labelled K1 and K2, that are associated with the edge carbon site. Once again, the edge $\pi^*$ peak is not present because this carbon atom is $sp^3$-bonded to three hydrogen atoms and one other carbon atom. The K1 peak has an $X$–$Y$ component from site 1 and also a significant $Z$-component from all the carbon atoms, and hence is assigned to a mixture of $\pi^*$ and the $\sigma^*(C–H)$ bond. The K2 peak is almost entirely due to site 1 and the $Z$-direction and is therefore associated with a $\pi^*(C–H)$ bond.

4. Discussion and conclusions

Atomic resolution core-loss EELS has been achieved experimentally [11] and used to study graphene edges. The advantage of the ab initio approach to core-loss EELS is that it is possible, via a combination of analyses as demonstrated above, to accurately reproduce and understand the experimental spectra. In an anisotropic material such as a GNR, the use of polarized core-loss EELS is a very useful source of extra spatial information, and combined with symmetry resolved electronic PDOS, can be used to identify the origins of all the primary features. In this way, polarized atom-resolved core-loss EELS can be used as a fingerprint for structure determination.

As an example of the power of core-loss EELS as a fingerprint method, consider the case of carbon triple bonds: the first sharp peak at the edge carbon site in polarized core-loss EELS in the $X$-direction is a clearly identifiable feature seen in figures 3 and 12. Similarly, in the case of hydrogenation, the first sharp peak at the edge carbon atom in the $X$- and $Y$-directions can be readily identified in figures 6, 15, 20, etc.

From an experimental point of view, this combination of atomic-resolution and polarization presents a significant challenge. Atomic resolution core-loss EELS normally involves use of a convergent electron probe, but in that case the polarization information may be mixed, and instead separate polarization-dependent core-loss EELS measurements using a less convergent beam over a larger area is required. However, there is an alternative way of combining site-resolved and polarization-resolved core-loss EELS using two different convergence angles and use the difference signal to extract the anisotropic information [12, 13].

Finally, to summarize the key points about the core-loss EELS spectra for the different structures considered, the unpolari-
carbon atom is shown in figure 21. The spectra are arranged vertically in order of increasing energetic stability, with di-hydrogenated AGNR at the top, and unhydrogenated, unreconstructed ZGNR at the bottom. Whilst the general trends are clear, this also shows that peak position alone is insufficient to unambiguously identify the structure, and that the polarization analysis is an essential requirement.

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