Enhanced Anomalous Hall Effect in Magnetic Topological Semimetal Co$_{3}$Sn$_{2−x}$In$_{x}$S$_{2}$

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We study the anomalous Hall Effect (AHE) of single-crystalline Co$_{3}$Sn$_{2−x}$In$_{x}$S$_{2}$ over a large range of indium concentration $x$ from 0 to 1. Their magnetization reduces progressively with increasing $x$ while their ground state evolves from a ferromagnetic Weyl semimetal into a nonmagnetic insulator. Remarkably, after systematically scaling the AHE, we find that their intrinsic anomalous Hall conductivity (AHC) features an unexpected maximum at around $x = 0.15$. The change of the intrinsic AHC corresponds with the doping evolution of Berry curvature and the maximum arises from the magnetic topological nodal-ring gap. Our experimental results show a larger AHC in a fundamental nodal-ring gap than that of Weyl nodes.

I. INTRODUCTION

The interplay between topology and magnetism is emerging as the new frontier in fundamental quantum physics [1–8]. A rich variety of topologically nontrivial states with time-reversal symmetry breaking have been realized in many material systems [4, 13]. One striking example is the magnetic Weyl semimetal (WSM) featuring the linearly dispersive band-touching points called Weyl nodes, analogous to the massless relativistic Weyl fermions in high energy physics. As a signature of Weyl nodes, large intrinsic anomalous Hall effect (AHE) has been observed in many candidates of magnetic WSMs [14, 18, 21]. Large AHE can stem from different types of hot zones of Berry curvature in momentum space such as Weyl nodes and topological nodal rings [22]. Understanding the relationship between the AHE and electronic structure in magnetic WSMs is crucial for designing functional quantum materials. However the hot zones of Berry curvature are hard to be discerned by measuring the AHE because it is sensitively dependent on the Fermi level ($E_{F}$) and spin splitting.

Tuning the chemical potential by doping is a powerful tool to address the relationship between the AHE and Berry curvature change in a variety of magnetic materials [23, 26]. For topological semimetals, however, this strategy is less proven efficient because other effects accompanied by the chemical doping such as electron scattering may also affect the AHE significantly. In this paper we focus on a series of indium-substituted Co$_{3}$Sn$_{2}$S$_{2}$ with a progressively changed chemical potential. Co$_{3}$Sn$_{2}$S$_{2}$ is one of the very few compounds that has been confirmed to be magnetic WSM in experiment [27, 28]. This compound possesses kagomé layers of Co atoms stacking in rhombohedral setting (Fig. 1(a)) and shows a half-metallic ferromagnetic (FM) ground state with a Curie temperature ($T_{C}$) of 177 K and spontaneous magnetic moment of 0.3 $\mu_B$/Co. The electronic structure of Co$_{3}$Sn$_{2}$S$_{2}$ forms two sets of linear band crossing points of nodal ring slightly above and below $E_{F}$ if spin-orbit coupling (SOC) is not considered. When SOC is taken into account, the Weyl nodes are generated from the nodal rings split above $E_{F}$ while an indirect SOC gap forms below $E_{F}$ (Fig. 1(b)). As a signature of the topological electron band, large intrinsic AHE has been observed in pristine Co$_{3}$Sn$_{2}$S$_{2}$ [21, 21].

We investigate the AHE in a series of Co$_{3}$Sn$_{2−x}$In$_{x}$S$_{2}$ where increasing indium substitution effectively lowers the chemical potential. The indium substitution drives a transition from an FM WSM to a non-magnetic insulator in Co$_{3}$Sn$_{2−x}$In$_{x}$S$_{2}$, which can be well understood as the result of electron depopulating from the half-metallic band [22]. Remarkably, we find an enhanced anomalous Hall conductivity (AHC) up to 2500 $\Omega^{-1}$cm$^{-1}$ when $x = 0.15$, compared to a monotonically damped magnetization by increasing $x$. By scaling the AHC, we extract...
the intrinsic part which is well reproduced by the Berry curvature of Co$_3$Sn$_2$S$_2$. Our results demonstrate that the SOC-induced nodal-ring gap can generate a larger AHC than that of the Weyl node in magnetic WSMs. This finding highlights a way to enhance the AHE in magnetic topological semimetals.

II. EXPERIMENTAL RESULTS

Single crystals of Co$_3$Sn$_2$-xIn$_x$S$_2$ were grown by the Bridgeman technique [30]. The stoichiometry and high quality of the crystals were confirmed by energy dispersive X-ray spectroscopy (EDS) and the structural refinement based on powder X-ray diffraction. The lattice parameters $a$ and $c$ show linear dependence on the indium concentration for $0 \leq x \leq 0.8$ (Fig. 1(c)), in good agreement with previously reported results [29, 31–33]. Figure 1(d) shows that the $x$ determined by EDS equals the initial indium concentration in the molten solution, verifying the crystal’s homogeneity. An X-ray Laue back reflection photograph confirms the high quality and orientation of the single crystals (inset of Fig. 1(d)). Our single crystal X-ray diffraction on representative samples confirms that the indium atoms preferentially substitute the interlayer tin atoms [29, 32, 34] and the kagomé lattice remains intact when $x < 1$ [35].

The magnetic and electrical transport properties for several single crystals with representative indium concentration are shown in Fig. 2. While the $T_C = 176 \pm 1$ K and the saturated magnetization at 2 K ($M_s = 0.3 \mu_B$/Co) for pristine Co$_3$Sn$_2$S$_2$ are maximal for the whole series, both two values are monotonically suppressed by the indium substitution [34, 36, 37]. When $x = 1$, the sample exhibits non-magnetic behavior. In Fig. 2(b), we plot temperature dependent resistivity for several Co$_3$Sn$_2$-xIn$_x$S$_2$ samples. As previously reported [21, 24], the resistivity at zero magnetic field ($\rho_{xx}$) shows a metallic profile with a kink around $T_C$ when $x \leq 0.8$. Furthermore, the resistivity for the $x = 1$ sample has an insulating profile, showing a metal-to-insulator transition with increasing $x$. This transition is the result of depopulation of the half-metallic band in which the indium substitution progressively lowers the chemical potential by removing one electron for each substituted tin atom (Fig. 1(d)) [34, 36, 37]. The electronic structure of the series approximates to the rigid band of Co$_3$Sn$_2$S$_2$, which gives us an opportunity for addressing the relation between the Berry curvature and AHE as the chemical potential changes in a wide range.

The magnetic field dependence of Hall resistivity $\rho_{yx}$ at 2 K for Co$_3$Sn$_2$-xIn$_x$S$_2$ are shown in Fig. 2(c). The observed $\rho_{yx}$ comprises a field dependent ordinary term and an anomalous term:

$$\rho_{yx} = \rho_{yx}^O(B) + \rho_{yx}^A(M)$$

where $B$ is the induction field and $\rho_{yx}^O$ is the anomalous Hall resistivity following the magnetic hysteresis loops with sharp switching. The $\rho_{yx}^O(B)$ for the pristine sample shows a nonlinear field dependence at 2 K, which is a typical two-band feature [20]. For indium-substituted samples when $x < 0.7$, $\rho_{yx}^O(B)$ shows a linear dependence that can be interpreted by a single-band model. Figure 2(d) and inset plots $\rho_{yx}$ as the zero-field extrapolation.
of the high-field data and the extracted carrier densities, respectively. The hole density \( p = 9.8 \times 10^{19} \text{ cm}^{-3} \) is increased by a factor of ~170 when \( x \) increases from 0 to 0.6. The Hall signals for \( x = 0.7 \) and 0.75 show a two-band feature indicating a \( p-n \) transition onset. Further substitution significantly decreases the carrier density in insulating samples.

The anomalous Hall resistivity \( \rho_{yx}^A \) shows a significant enhancement near \( x = 0.1 \) and is then continuously suppressed until vanishing at \( x > 0.8 \). The maximum of \( \rho_{yx}^A \) is increased by a factor of 4 compared to pristine Co$_3$Sn$_2$S$_2$. It is clear that the variation of \( \rho_{yx}^A \) at 2 K does not follow the trend of the magnetization and carrier density. The \( p-n \) transition around \( x = 0.75 \) also does not affect the sign of \( \rho_{yx}^A \). We calculate the AHC for the whole series at different temperatures by using \( \sigma_{xy}^A = \frac{\rho_{yx}^A}{\rho_{xx}^2 + \rho_{xx}^2} \) (Fig. 3(a)). The \( \sigma_{xy}^A \) for pristine Co$_3$Sn$_2$S$_2$ is 850 \( \pm \) 200 \( \Omega^{-1} \text{cm}^{-1} \) at 2 K and remains nearly unchanged below 100 K, in good agreement with the previous results of the intrinsic AHE [29]. For \( x = 0.15 \), \( \sigma_{xy}^A \) becomes enhanced to 2500 \( \pm \) 500 \( \Omega^{-1} \text{cm}^{-1} \) at 2 K. Unlike the pristine sample, \( \sigma_{xy}^A \) for indium-substituted samples continuously increases with decreasing temperature, which indicates that part of \( \sigma_{xy}^A \) is related with scattering events.

III. DISCUSSION

We now disentangle the intrinsic and extrinsic contributions to the AHE. The anomalous Hall resistivity can be written as:

\[
\rho_{yx}^A = (\alpha \rho_{xx}^2 + \beta \rho_{xx}^2) \cdot M(T) \tag{2}
\]

in which the first term is linearly dependent on the resistivity, representing the extrinsic skew scattering contribution. The second term is quadratically dependent on the resistivity and represents an intrinsic plus side-jump contribution in the AHE. Both parts have a linear dependence on magnetization [38,39] and the parameters \( \alpha \) and \( \beta \) can therefore be obtained by plotting \( \rho_{yx}^A/M \rho_{xx} \) versus \( \rho_{xx} \), as shown in Fig. 3(b). The data shows good linearity at low temperatures for all samples and we can extract the intercept \( \alpha \) and slope \( \beta \) and calculate the skew scattering and intrinsic plus side-jump AHC at 2 K. Figure 3(c) shows that the intrinsic plus side-jump AHC has a maximum up to 1500 \( \pm \) 300 \( \Omega^{-1} \text{cm}^{-1} \) at \( x = 0.15 \), approximately twice as large as the pristine case. As comparison, the skew-scattering AHC \( (\sigma_{xy}^{sk}) \) also shows a broad maximum near \( x = 0.15 \) and then slowly decreases with increasing \( x \). Previous studies have reported the AHE in a variety of chemical compositions [23,26], but the non-monotonic change of the AHC is less observed in topological semimetals.

To shed light on the non-monotonic change in the AHC, we compare the extracted intrinsic plus side-jump AHC with the calculated energy-dependent AHC \( (\sigma_{xy}^{int}) \) in accordance to the Berry curvature of pristine Co$_3$Sn$_2$S$_2$ in Fig. 4(a). The \( \sigma_{xy}^{int} \) has a similar profile with respect to energy as the experimental data: it is enhanced below \( Eg \) with a maximum of \( \sim 1000 \Omega^{-1} \text{cm}^{-1} \) and then drops to nearly zero at \( -270 \text{ meV} \). The large \( \sigma_{xy}^{int} \) is attributed to hot zones of Berry curvature in the Brillouin zone. Figure 3(b)-(d) show the Berry curvature distribution projected to the \( k_x-k_y \) plane at three different energies of -60, 0 and \( 60 \text{ meV} \), respectively. These energy levels correspond to the \( E_g \) of the SOC gap at high-symmetry line, for the pristine sample and that of the Weyl nodes respectively. The color maps show different origins of hot zones: the main contributions from the Weyl nodes and the gapped nodal rings, plus some negligible contribution from other bands. The contributions from the Weyl nodes and nodal rings are comparable as the \( E_g \) is located at \( 60 \text{ meV} \). With decreasing \( E_g \), the Berry curvature contribution from
FIG. 4. (a) Black solid line: calculated $\sigma^{\text{int}}_{xy}$ for Co$_3$Sn$_2$S$_2$ with respect to the chemical potential. Red dots with error bar: experimental results of the intrinsic plus side-jump AHC for Co$_3$Sn$_{2-x}$In$_x$S$_2$ at 2 K. The chemical potential is inferred from rigid band approximation (see Fig. 1d). Blue solid line: the AHC for massive Dirac model. (b), (c) and (d): Berry curvature distribution projected to the $k_x$-$k_y$ plane for Co$_3$Sn$_2$S$_2$ at the energy of -60, 0 and 60 meV, respectively. The color bar on right presents the Berry curvature intensity. NR and WP represent nodal ring and Weyl point, respectively.

The nodal rings is enhanced, compensating the reduced contribution from the Weyl nodes. The total $\sigma^{\text{int}}_{xy}$ has a maximum around -60 meV, in agreement with our transport experiment.

Our measurements and calculations show that the small SOC gap in Co$_3$Sn$_2$S$_2$ generates a large AHC which is comparable to a quantized value. To illustrate this point clearly, we compare this result to the AHC in a massive Dirac model which can be realized in a kagomé lattice of the magnetic atoms. The corresponding AHC equals $\sigma_{xy}^{0} = 3 \times \frac{e^2}{\hbar c} = 881 \Omega^{-1}\text{cm}^{-1}$ with the quantized Hall conductance $e^2/h = 3.87 \times 10^{-5} \Omega^{-1}$ and $c = 13.176$ Å for a fictitious lattice hosting massive Dirac cone. The factor 3 is introduced because the unit cell of Co$_3$Sn$_2$S$_2$ contains three layers of Co kagomé lattice. This value is slightly smaller than $\sigma_{xy}^{0}$ and the experimental results for Co$_3$Sn$_{2-x}$In$_x$S$_2$ in the region of $-60 \pm 25$ meV. In a large energy scale, however, the profile of AHC in this simple massive Dirac model is close to the experimental result.

Part of the discrepancy between the calculated $\sigma^{\text{int}}_{xy}$ and experimental results may be attributed to the side-jump contribution which also has a quadratic dependence of $\rho_{xx}$ and is therefore difficult to distinguish from the intrinsic one. However the side-jump contribution should be smaller than $e^2/hc$ and the intrinsic contribution is dominant in the total AHC. The side-jump contribution can be estimated as $\frac{e^2}{\hbar c} \frac{\varepsilon}{\mu}^{25}$ where $\varepsilon_{SO}$ is the strength of the SOC. Given $\varepsilon_{SO}$ is about 50 meV, we estimate $\sigma^{sk}_{xy}$ about 50 $\Omega^{-1}\text{cm}^{-1}$, much less than the intrinsic contribution. Another point of concern is the $\sigma^{sk}_{xy}$ which also exhibits a broad maximum near $x = 0.15$. Due to multi-variable complexity including spin-orbit interaction, scattering strength and disorder density, calculating the energy dependence of $\sigma^{sk}_{xy}$ in Co$_3$Sn$_{2-x}$In$_x$S$_2$ is difficult. We briefly discuss the origin of non-monotonic change of $\sigma^{xy}_{xy}$ as below. As shown in Fig. S5 in SI, $\sigma^{sk}_{xy}$ is linearly dependent on the carrier mobility $\mu$ when $x > 0.15$. In contrast $\sigma^{sk}_{xy}$ starkly deviates from the linear dependence on the mobility as long as $x < 0.15$. This deviation is not unexpected because the chemical potential crosses the SOC gap when $x$ is about 0.15. Therefore the non-monotonic change of $\sigma^{xy}_{xy}$ in Co$_3$Sn$_{2-x}$In$_x$S$_2$ reflects the fact that Fermi energy across the SOC gap near $x = 0.15$. We notice that the discontinuous change in $\sigma^{sk}_{xy}$ near the SOC gap was shown for some model systems. The detailed electronic structure for this alloy system asks for elaborations in the future.

IV. CONCLUSION

In summary, we have investigated the AHE in a series of Co$_3$Sn$_{2-x}$In$_x$S$_2$ single crystals which change from an FM WSM to a non-magnetic insulator as $x$ increases. This transition can be well described as the result of band depopulation by removing one electron per formula unit from the pristine Co$_3$Sn$_2$S$_2$. We separate the intrinsic and skew-scattering AHC and find that both do not follow the change of magnetization or carrier density. The intrinsic AHC obtained in experiment is consistent with the non-monotonic change of Berry curvature of Co$_3$Sn$_2$S$_2$ dependent on $E_F$. The SOC-induced nodal-ring gap contributes a strong hot zone of Berry curvature which induces an enhanced AHC. Our work clarifies the source of the large AHC in the first experimentally confirmed magnetic WSM Co$_3$Sn$_2$S$_2$ and provides a path to enhance the AHE in other topological materials.

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