Simulation of the gastric digestion of proteins of meat bolus using a reaction–diffusion model
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**ABSTRACT:**

A reaction–diffusion mathematical model has been developed to predict the gastric digestion of meat proteins. The model takes into account pepsin diffusion and proton diffusion in bolus particles and the pH buffering capacity of the meat. The computations show that size of bolus particles and change in gastric pH have a substantial effect on the percentage of protein digested in the stomach and that the pH buffering capacity of the meat has to be accounted for to properly calculate the gastric digestibility of meat. The intensity of surface transfers between stomach fluid and bolus particle has a significant impact on protein digestibility, whereas the variations in pepsin content in the stomach between individuals appears to have little effect on protein digestibility. From a nutritional standpoint, the simulations show that meat protein digestibility is high in normal physiological stomach conditions. However, in a situation where masticatory capacity, hydrochloric acid secretion and gastric motor function performances are reduced, such as with advancing age, protein digestibility rapidly decreases, ultimately leading to near-zero digestibility value in the stomach in extreme cases.

**HIGHLIGHTS:**

- Mathematical model predicts the gastric digestion of meat
- Quantification of the effects of physiological factors on meat digestion
- Protein digestibility is driven mainly by gastric pH and bolus particle size

**KEYWORDS:** transfer, kinetics, model, stomach, beef meat, pepsin, digestibility
List of symbols used:

D: mass diffusivity of pepsin or proton in water (m².s⁻¹)

E: enzyme concentration (U.mg⁻¹)

EₚH: active enzyme concentration, which is pH-dependent (U.mg⁻¹)

Eₚmax: fraction of active enzyme able to reach all the cleavage sites available on the protein (linked to pH and to maximum number of cleavage sites available)

EₚH=2: maximum value of Eₚmax for raw beef meat as measured on extracted myofibrils immersed for a very long time in a solution of pepsin at pH 2 (optimum pH for pepsin activity); used as a reference value to calculate the digestibility ratios σ, σ̅(t), ̄σ

H⁺: molar concentration of hydrogen ions (mol.l⁻¹)

kHCl: mass transfer coefficient of hydrochloric acid at the gastric fluid–bolus particle interface (m.s⁻¹)

kPepsin: mass transfer coefficient of pepsin at the gastric fluid–bolus particle interface (m.s⁻¹)

Kₐ₁: First pepsin dissociation constant (bi-acid behavior)

Kₐ₂: Second pepsin dissociation constant (bi-acid behavior)

KₜH: coefficient of meat pH buffering capacity

L: pseudo reaction rate constant, which depends on lᵢ and on kinetic rate constants of the absorption and desorption reactions of the cleavage sites

Lₗₖ: characteristic length, in our model equal the diameter of a meat bolus particle, Size (m)

lᵢ: kinetic rate constant of the formation of peptides and amino acids from protein cleavage (min⁻¹)

P: relative concentration of the peptides and amino acids formed from protein cleavage

pH: potential of hydrogen (pH unit)

pKₐ₁ and pKₐ₂: equal to -log₁₀(Kₐ₁) and -log₁₀(Kₐ₂), respectively

r: radius of a meat bolus particle (mm)

Re: Reynolds number for bolus particles immersed in the gastric fluid (= (ρ * v * Lₗₖ)/μ)

Sc: Schmidt number for the bolus particles immersed in the gastric fluid (= μ/(ρ * D))
Sh: Sherwood number for the bolus particles immersed in the gastric fluid (\(= \frac{k}{D/L_{car}}\))

Size: diameter of a meat bolus particle (mm)

t: time (s)

t_{end}: time period from ingestion to the end of gastric emptying (s)

t_{lag}: time period from ingestion to the end of the lag phase of gastric emptying (s)

t_{\sigma=50\%}: digestion time necessary to reach 50\% digestibility of the proteins contained in the bolus particles relative to the maximum digestibility of extracted myofibrillar proteins (\(E_{max}^{*pH=2}\)) (s)

t_{\sigma=75\%}: digestion time necessary to reach 75\% digestibility of the proteins contained in the bolus particles relative to the maximum digestibility of extracted myofibrillar proteins (\(E_{max}^{*pH=2}\)) (s)

V: meat particle volume (m³)

\(\delta_{max}\): product of \(E_{max}^{*pH}\) and of the calibration constant of the spectrophotometer

\(\Delta\): Laplace operator; in spherical coordinates without angular variations, may be simplified to \(\Delta = \frac{\partial^2}{\partial r^2} + \frac{2}{r} \frac{\partial}{\partial r}\)

\(\mu\): dynamic viscosity of the gastric fluid (Pa.s)

\(v\): velocity of the gastric fluid around meat bolus particles (mm. s⁻¹)

\(\rho\): density of the gastric fluid (kg. m⁻³)

\(\sigma\): local digestibility ratio inside a meat particle relative to the maximum protein digestibility measured on extracted myofibrils immersed in a pepsin solution at pH 2 (% of \(E_{max}^{*pH=2}\))

\(\bar{\sigma}(t)\): digestibility of a meat particle, at a given time \(t\) of digestion, ratioed to the maximum protein digestibility measured on extracted myofibrils immersed in a pepsin solution at pH 2 (% of \(E_{max}^{*pH=2}\))

\(\bar{\sigma}\): mean digestibility ratio for a given bolus particle size after a given gastric residence time(% of \(E_{max}^{*pH=2}\))

\(\Phi\): mass transfer of pepsin or of protons at the meat particles–gastric fluid interface (mol.m⁻². s⁻¹)

**Superscripts:**

+: gastric conditions most favorable to digestibility

-: gastric conditions least favorable to digestibility
o: most probable average gastric conditions

Subscripts:

Free: ions which are not bonded to proteins, and are able to diffuse

Gastric: relative to the value in the gastric fluid, outside meat

HCl: relative to hydrochloric acid

Pepsin: relative to pepsin gastric enzyme
Simulation of the gastric digestion of proteins of meat bolus using a reaction–diffusion model

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INTRODUCTION

Meat is a major source of dietary proteins that provide all the essential amino acids. The digestion rate of the proteins is known to be the main determinant of their assimilation in the diet, especially for sarcopenia-prone elderly people. Human digestion of foods is a multi-operation process in which mastication and gastric digestion have a major impact. The consumer’s mastication capacity and the food’s texture affect the average size and distribution of the particles in the bolus, after which the stomach plays a major role in bolus particle breakdown, mixing and sieving, as well as in the acido-enzymatic destructuration of proteins. The stomach needs a low pH to activate pepsin, one of the main digestive enzymes, which cleave proteins into peptides and leads to amino acids such as phenylalanine, tryptophan and tyrosine. Most data on the gastric digestibility of meat has come through in vitro or in vivo studies on humans or animals. However, in vivo measurements only give a global indication of food digestibility while in vitro experiments, even when performed in sophisticated systems, are limited in mimicking the physiology of the human tract. Mathematical modeling of digestion offers an alternative approach that can provide information that is time-intensive and sometime impossible to obtain experimentally in vitro and in vivo.

Myofibrillar proteins contribute 60% of meat protein content. Pepsin digestibility of myofibrillar proteins has already been modeled in vitro by Kondjoyan et al. but their work was only a first approach and their model’s results were not directly applicable to the digestion of proteins contained in the meat particles of the bolus. As myofibrils are hundred-micron-sized bodies, the diffusion of protons and pepsin and the food buffering capacity of the meat can be assumed to be of negligible effect. pH and pepsin concentration in the meat were thus assumed to be the same as in the surrounding fluid. In fact, this is not the case for the millimeter-sized particles contained in the bolus.

This paper reports simulation work predicting the effects of pepsin concentration, pH variations and meat particles size on the gastric digestion of proteins contained in bolus particles using a reaction–diffusion mathematical model. Kondjoyan et al. showed that cooking also has an impact on the kinetics and maximum digestibility of proteins, but that pH variation in the stomach had a much bigger effect (Kondjoyan et al., Fig. 4). Thus we focus on the impact of factors related to mastication and
gastric digestion of raw meat and not on cooking. But the approach proposed remains fully transposable to cooked meat pieces.

1 **MATHEMATICAL MODELLING**

1.1 **MODEL MAIN ASSUMPTIONS**

The model principles are described in Fig. 1. Modelling begins at the entrance of the stomach. The solid bolus entering the stomach is assumed not to be a single coherent body but a collection of unlinked food particles which separate and rapidly get mixed with the gastric fluid due to gastric contractions. This assumption is supported by the fact that during wet sieving, that is used to determine particle sizes after mastication, food particles separate indicating a low inter-particles bonding. The model is focused on the digestion of particles which size is greater than half a millimeter. The median size of the food particles in the bolus and their size distribution are taken from literature data. The particle size is assumed to remain the same during gastric digestion. Under physiological conditions, several thousand food particles in the micron-size range may also be present in the liquid phase of the bolus at the entrance of the stomach. The present simulations do not account for these particles, which represent a relatively low weight-by-mass proportion of the bolus. In the stomach, the food particles are subjected to the gastric fluid whose pH varies during digestion while Pepsin concentration is assumed to be constant.

Gastric digestion of millimeter size food particles is limited by the diffusion of pepsin inside the particles. In fact pepsin activity is also dependent on pH. Thus particle digestion is also affected by the diffusion of the protons in the particle and by the buffering capacity of the food.

The mathematical approach followed in the paper is classically used in food engineering. Mass transfers of pepsin and of protons are described by Fickian diffusions inside meat spherical particles; the initial pH of these particles being 5.5. The mathematical boundary condition chosen in the paper to describe the exchanges at the surface of these spherical particles is a Neumann-type equation. This equation presents the advantage to take indirectly into account the effect of particle movement in the stomach on the surface exchanges using a mass transfer coefficient, which value can be assessed using food engineering correlations and physiological measurements. Boundary conditions and diffusions equations lead to local pepsin and proton concentrations inside each food particle. A buffering term is added in the mass transfer of protons to take into account the effect of food composition on the local value of pH inside the particle. Local pepsin concentration and pH value are used to calculate a local digestibility index which varies with time. Time variation of the particle digestibility is calculated by averaging the local index in the entire volume of the particle. This value was compared with the
maximum obtainable protein digestibility, which is achieved for a meat particle with zero buffering capacity left for an infinite time totally immersed in a gastric solution held constantly at pH 2 and with a very high pepsin concentration. In such an optimal situation, we would have maximum digestion for all the proteins contained in the meat particle since the pepsin could reach all the cleavage sites available at a maximum active enzyme concentration.

The following sections detail the equations, the values of the model parameters and the calculations procedure used to simulate the digestion process. As we did not find reliable parameters to describe the buffering effect limiting the pH of the meat particle, a set of experiments was specially designed to quantify it. The reliability of the model assumptions is discussed during the presentation of the simulated results.

1.2 EQUATIONS

1.2.1 DIFFUSION OF ACID AND PEP SIN

Fick’s second law used to describe the diffusion of the pepsin within the meat bolus particles was written as eq. 1.

\[
\frac{\partial E}{\partial t} = D_{\text{Pepsin}} \Delta E \quad (\text{eq. 1})
\]

The Neumann boundary condition imposed on the partial differential equation 1 at the meat particle–gastric fluid interface was eq. 2.

\[
\Phi_{\text{Pepsin}} = k_{\text{Pepsin}} (E - E_{\text{Gastric}}) \quad (\text{eq. 2})
\]

\[k_{\text{Pepsin}}\] was the mass transfer coefficient value used to describe the pepsin exchanges at the surface of the particle.

Pepsin activity is known to vary with pH depends on the type of pepsin and on the protein substrate. pH–pepsin activity curves exist in model proteins like albumin or hemoglobin.\(^{27,28}\) The pepsin activity curve has an optimal pH above or below which it decreases. The decrease in activity of the enzyme between pH 2 and pH 5 is a lot less strong for human pepsin degrading albumin than for porcine pepsin degrading hemoglobin; the effect of substrate being determinant (the optimum pH for maximum pepsin activity being 1.5–2.5 for hemoglobin vs 3 for albumin\(^{29}\)). The function used in this study to describe pepsin activity was the function determined by Pletschke et al.\(^{28}\) for the reaction of hemoglobin with porcine and ostrich pepsins. The rationale justifying this choice is that this same function has already been validated for the substrate under study, i.e. beef myofibrillar proteins\(^{24}\), which form about 60% of total meat protein\(^{23}\). Furthermore, studies on human pepsin classically use porcine pepsin as a proxy standard due to its availability and similarity\(^{30}\). This function causes pepsin activity to drop rapidly as pH climbs from 2, with a 50%-plus activity reduction already at pH 3.
The local-point variations in pH inside these particles, which depends on the proton diffusion in the matrix and on the pH buffering capacity was described by the following system of equations 3.

\[
\begin{align*}
\text{eq. 3a} & : & \quad \text{pH} & = -\log_{10}[H_{\text{Free}}^+] \\
\text{eq. 3b} & : & \quad \frac{\partial H_{\text{Free}}^+}{\partial t} & = D_{\text{HCl}} \Delta H_{\text{Free}}^+ - f(H_{\text{Free}}^+)D_{\text{HCl}} \Delta H_{\text{Free}}^+ \quad (\text{eq. 3b})
\end{align*}
\]

In equation 3b, term I represents Fickian diffusion linked to the concentration gradient of H\(^+\) ions whereas term II represents the decrease in this same concentration due to the composition of the meat media, where \(f(H_{\text{Free}}^+)\) is a function characterizing the buffering capacity of the meat. The pH buffering of meat is induced by the bonding of some hydrogen ions with proteins; the ions which remain unbounded being able to diffuse within the meat particles. The subscript “Free” has been added in the equations to represent these unbounded ions. When food comes into contact with gastric juice, there are other ion exchanges than H\(^+\) that take place between the meat and its environment, but these exchanges are not considered in our model.

The literature has employed various approaches to account for \(f(H_{\text{Free}}^+)\), ranging from introducing an apparent diffusivity value into Fick’s law (equal to \(D_{\text{HCl}}(1 - f(H_{\text{Free}}^+))\), \(f(H_{\text{Free}}^+)\) being constant)\(^{31}\) to constructing experimental relations to link buffering capacity to the composition and biochemical characteristics of different muscles.\(^{32}\) In this last study, buffering capacity was experimentally observed to vary almost linearly with pH.

The Neumann boundary condition was eq. 4.

\[
\Phi_{H_{\text{Free}}^+} = k_{\text{HCl}}(H_{\text{Free}}^+ - H_{\text{Free,Gastric}}^+) \quad (\text{eq. 4})
\]

where \(k_{\text{HCl}}\) was the mass transfer coefficient of hydrochloric acid at the meat bolus particle–gastric fluid interface.

\(k_{\text{HCl}}\) and \(k_{\text{Pepsin}}\) were estimated based on data found on the dynamic properties of gastric fluid and correlations derived from the literature, or identified based on our experimental data also used to determine the buffering capacity of meat. Under the hypothesis of spherical bolus particles fully immersed in a homogeneous gastric solution, there is no angular variation for concentrations.

From among the multitude of potentially workable correlations, we tested two classical correlations co-connecting the Sherwood number (Sh), Reynolds number (Re) and Schmidt number (Sc) in order to assess the impact of this choice on the calculations of the digestibility of proteins.
The Sherwood, Reynolds and Schmidt dimensionless numbers can be related to the gastric flow conditions around meat bolus particles through eq. 5, 6 and 7.

\[
Sh = \frac{k}{(D/L_{\text{car}})} \quad \text{(eq. 5)}
\]

\[
Re = \frac{(\rho \ast v \ast L_{\text{car}})}{\mu} \quad \text{(eq. 6)}
\]

\[
Sc = \frac{\mu}{(\rho \ast D)} \quad \text{(eq. 7)}
\]

The first correlation between those dimensionless numbers (eq. 8) corresponds to forced convection around a sphere\(^3\), whereas the second correlation (eq. 9) corresponds to a simplified mass transfer in a fluidized bed\(^3\), simplified because it neglects the Archimedes number. The rationale justifying this simplification is that there is little difference in density between gastric fluid and food bolus.

\[
Sh = 2.0 + 0.6 \ast Re^{1/2} \ast Sc^{1/3} \quad \text{(eq. 8)}
\]

\[
Sh = 0.14 \ast Re^{1/3} \ast Sc^{1/3} \quad \text{(eq. 9)}
\]

The eq. 10 finally providing the mass transfer coefficients ensues from eq. 5.

\[
k = Sh \ast (D/L_{\text{car}}) \quad \text{(eq. 10)}
\]

The characteristic length is the size of the meat particle.

The details on the gastric flow conditions chosen to calculate \(k_{\text{pepsin}}\) and \(k_{\text{HCl}}\) are given in section 3.2. Note that since ranges of Reynolds numbers in the stomach are directly available in the literature, eq. 6 has not been directly used in this paper.

\subsection{1.2.2 DIGESTION BY ACTIVE PEP SIN}

In order to predict digestibility, these equations were completed by the reaction model of pepsin digestibility of myofibrillar proteins from beef muscle developed by Kondjoyan et al.\(^2\)\(^4\) In this reaction model, the pH–dependent activity of pepsin behaved like that of a diacid (H\(_2\)E). Enzyme concentration was thus split between the active pH-dependent component \(E^{PH}\) and the total enzyme concentration \(E\) based on the following relation (eq. 11):

\[
\frac{E^{PH}}{E} = \frac{HE^{-}}{H_{2}E + HE^{-} + E^{2-}} = \frac{1}{1 + 10^{-pH} \ast \frac{K_{a1}}{10^{-pH} \ast K_{a2}}} \quad \text{(eq. 11)}
\]

The fraction of active enzyme able to reach all the cleavage sites available on the protein, will be written in what follows as \(E_{\text{max}}^{*PH}\). It depends on prior thermal treatment of the meat, and is taken, here, as equal to that of the raw meat.

In practice, the value of \(E_{\text{max}}^{*PH}\) was computed from an optical density value that served to track the quantity of cleavage products, \(P\), amino acids or peptides, derived from the digestion of myofibrillar
proteins. The linkage between constant $E_{max}^{pH}$ and the measurement was determined via a second constant $\delta_{max}$ that accounted for calibration of the instrument (Kondjoyan et al.24; Table 1). Constant $E_{max}^{pH}$ accounted for the amount of active enzyme that is pH-dependent via eq. 11.

The proportion of cleavage sites reached, leading to the formation of digestion-derived products, written $P$, in mass of protein digested ratioed to total mass of proteins in the meat, followed a first-order reaction (eq. 12)$^{24}$, where $l_f$ is the kinetic constant of the reaction:

$$P(t) + \frac{1}{l_f} \frac{dP(t)}{dt} = E_{max}^{pH} \frac{E^{pH}}{E^{pH}+L} \quad (eq.\ 12)$$

The model developed$^{24}$ concerned myofibrillar proteins in solution for which pepsin diffusion and acid diffusion were not rate-limiting, resulting in a constant value of $E_{max}^{pH}$ in which the pH considered is the pH of the gastric juice.

The spatiotemporal variation in pH was added in the present model. This consequently made $E^{pH}$ into a variable that depended on the local enzyme and proton concentrations inside the meat. The equation solved at every point in the meat thus became (eq. 13):

$$P(t) + \frac{1}{l_f} \frac{dP(t)}{dt} = E_{max}^{pH} \frac{E^{pH}(t)}{E^{pH}(t)+L} \quad (eq.\ 13)$$

As time increases, the active enzyme concentration in the meat, $E^{pH}$, tends to be equal to the active enzyme concentration in the gastric fluid $E^{pH}_{Gastric}$. The value of this active pepsin concentration is maximum for $pH_{Gastric} = 2$. When enzyme concentration in the gastric fluid $E_{Gastric}$ is well above $L$—as is the case for the gastric conditions studied here—and the gastric fluid is at optimum pH, i.e. pH 2, the influence of the pseudo reaction rate constant $L$ becomes negligible.

Previous digestibility results were compared to the maximum value of the digestibility of meat proteins obtained in a previous paper using extracted myofibrils immersed in a pepsin solution at pH 2. This maximum digestion situation is written $E_{max}^{pH=2}$ in what follows, and serves as reference in the rest of the paper. The relative digestibility term $\sigma$ was introduced to quantify the effect of pepsin and proton diffusion in the meat and of its buffering capacity on the mean digestibility of the particles contained in the bolus, compared to what would have happened for myofibrils immersed in the pepsin solution at pH 2.

At a given point in time $t$, the mean value of $\sigma$ in volume $V$ of the meat particle equals (eq. 14).
\[
\sigma(t) = \frac{\int_{V} P(t) \, dV}{E_{\text{max}}} = \frac{\bar{P}(t)}{E_{\text{max}}} \quad \text{(eq. 14)}
\]

In a first approximation, as the time-course change in particle size is not yet studied, volume \( V \) is held constant.

In reality, the digestibility of the particle depends on residence time in the stomach. After ingestion of the bolus, the rate of gastric emptying starts with a lag phase during which there is very little emptying, followed by a linear phase of emptying.\(^{35-38}\) As this second phase is linear, the amount of particles exiting the stomach is constant over time. The mean digestibility of particles of a given size exiting the stomach, \( \bar{\sigma} \), can be calculated by eq. 15.

\[
\bar{\sigma} = \frac{\int_{t_{\text{lag}}^{\text{end}}} t \, \sigma(t) \, dt}{t_{\text{end}} - t_{\text{lag}}} \quad \text{(eq. 15)}
\]

\( t_{\text{lag}} \) and \( t_{\text{end}} \) being the end of the lag phase and the full emptying time respectively.

1.3 CALCULATIONS PROCEDURE

The equations for the pure diffusion of pepsin and protons (with only the term I in eq. 3b considered in a first stage) were discretized by a finite difference method using the second-order Crank-Nicolson numerical scheme that has the advantage of being numerically stable and accurate.\(^{39,40}\) Details of the discretization procedure are not given here but can be found in Heat Transfer\(^{41}\). The model was implemented using MATLAB\(^{\circledR} \) 2017a.

The function \( f(H_{\text{Free}}^+) \) was not determined directly but instead a stepwise approach was used during the Crank-Nicolson discretization (eq. 3b term II). A parameter \( K_H \) was introduced to decrease the local diffused proton concentration during a time step (eq. 16); this decreased concentration of proton being used for the calculus of diffusion during the next time step.

\[
\begin{align*}
\Delta t \quad \Delta t \\
pH_{t+\Delta t} - pH_t = K_H (-log_{10}[H_{\text{Free}}^+])_{t+\Delta t} + log_{10}[H_{\text{Free}}^+]_{t} \\
&= K_H (-log_{10}[H_{\text{Free}}^+])_{t+\Delta t} + log_{10}[H_{\text{Free}}^+]_{t} \\
\end{align*}
\quad \text{(eq. 16)}
\]

The local pepsin concentration and pH were used to calculate the local-point concentration of active pepsin (eq. 11) and digestion products (eq. 13).

The algorithm has been initialized at time = 0, by determining the free protons concentration in the meat based on the mean pH measured on fresh meat samples, i.e. \( pH_0 = 5.5 \) (eq. 17), through (eq. 18), whereas the initial concentrations of pepsin and digestion products \( P \) were assumed as nil.

\[
[H_{\text{Free}}^+]_0 = 10^{-pH_0} \quad \text{(eq. 18)}
\]
The local-point kinetics of the $P(t)$ values thus obtained were used to determine $\sigma(t)$ and $\bar{\sigma}$ from equations (14) and (15) by considering a homogeneous initial composition of the meat-bolus particles.

As parameter $K_e$ was a priori unknown, it was determined from a special purpose-designed experiment and a minimization procedure described below in section 2.

2 EXPERIMENTAL PROCEDURE USED TO VALIDATE THE PH BUFFERING PART OF THE MATHEMATICAL MODEL

The buffering capacity of the meat was determined using unidirectional measurement of pH in long meat cylinders mounted with the bottom in contact with a solution of HCl, as done previously. These results were completed by pH measurements carried out at different time points on thin slices of beef meat immersed directly in the acid solution.

Meat was coming from two beef muscles (Longissimus dorsi and Infraspinatus) that had been taken from Charolaise-breed cattle then vacuum-sealed and aged for 10 days at 4°C. Prior to the experiment, two 80 mm-long 30 mm-diameter cylinders were cut from in each muscle. These cylinders were each placed in a polyvinyl chloride (PVC) apparatus sat on top of a mesh to afford the flattest possible meat/acid contact surface (Fig. 2). pH of the hydrochloric acid solution was 2.0 ± 0.1. The solution was in contact with the bottom surface of the cylinder, and the apparatus was placed in an autoclave held at 37°C to mimic normal human body temperature. A sheet of aluminum foil was placed over the top of the apparatus to limit evaporation, and the solution was constantly shaken using a magnetic stirrer. The meat sample was mounted in such a way to be tightly squeezed by the edges of the plastic cylinder so as to limit capillary migration of acid along the sample edges.

Lebert & Daudin had shown that pH change inside the cylinder was slow, so we were forced to experiment long contact times of 6h, 18h and 24h in order to get measurable in-product pH change at a sufficient number of points over the height of the meat cylinder. These long trial times were not therefore physiologically representatives of gastric digestion, but were only used to validate the buffering part of the model.

At the end of the experiment, the meat cylinder was removed from the apparatus and frozen at -20°C for 40 minutes. A 10x10x80-mm parallelepiped was then cut from the center of the cylinder (to eliminate potential edge effects) and mounted in a cryostat and frozen to -53°C. A microtome (Microm HM 560, Thermo Scientific, France) was used to cut 500 µm-thick sections perpendicularly to the parallelepiped major axis. Then, each section was weighed, a mass of demineralized water
corresponding to 9 times the sample mass was added to obtain a 1/10 dilution, and the section-plus-water mixture was homogenized for 1 minute (Polytron PT-MR 2100, Kinematica, Switzerland). pH was measured using an InLab 427 puncture electrode (Mettler-Toledo, France) connected to a MA235 pH meter (Mettler-Toledo, France) plunged in the homogenate.

Complementary experiments on thin slices were carried out by plunging six 2 mm-thick 30 mm-diameter disks of meat sampled from the above muscles in a hydrochloric acid solution at pH 2.0 ± 0.1. Every 30 minutes, one of the disks was removed from the acid solution, weighed, and then measured for pH following the above protocol.

Fig. 3 reports the averages and ±2 standards deviation values obtained from these experiments.

3 STRATEGY USED TO CALCULATE THE RELATIVE DIGESTION OF PROTEINS
This paper set out to use the model described in part 1 to predict the effect of some human physiological factors on meat protein digestibility. However, uncertainty remains both on some of the model’s intrinsic parameters and on the values of the factors describing the physiological phenomena under study.

Table 1 lists (1) the main factors needed to calculate the effects of physiological phenomena on protein digestibility and their potential range of variation, and (2) the intrinsic parameters introduced in the model, their most probable values, and their range of variation.

3.1 REFERENCE VALUES OF THE FACTORS STUDIED IN THE PAPER
The first physiological factor introduced in the model is the particle sizes, which have been measured on boluses coming from the mastication of food products. Age-related loss of masticatory performance is expected to increase the amount of bigger particles.\(^{50}\) The values of median particle size in the solid phase of ready-to-swallow boluses range from under 1mm up to 6mm, with pork loin and frankfurters being near the upper bounds of that range.\(^{5,42}\) Given that these meat products share relatively similar mechanical properties to beef, we expected a similar median particle size range in the beef bolus considered in this study, with a range of variation between 3.5mm and 5mm depending on beef muscle type, maturation, and process.

The second physiological factor introduced is gastric pH, for which physiological fasting value ranges from 1.3 to 2.1.\(^{51}\) However, *Helicobacter pylori* infection and atrophic gastritis are associated with decreased acid secretion in the stomach, and the prevalence of these conditions is higher in older subjects.\(^{52}\) We studied age-related impairment of acidification for fasting pH values up to pH 2.9.
At the beginning of digestion, gastric pH is known to be much higher than its fasting value and to range from 4.5 to 5.8 depending on the meal’s composition and the consumer’s physiology. The time required to recover fasting pH level depends on food composition, food quantity, and food buffering capacity.\textsuperscript{53} In this study, the measurements of Malagelada et al.\textsuperscript{43} were chosen as a reference because the meal composition used in their paper is representative of that coming from an average American diet including 90 grams of beef meat.

The third physiological factor is pepsin concentration and activity in the gastric juice: pepsin secretion varies within the stomach, as the body of the stomach secretes significantly more pepsin than the antrum. For this study, we do not consider these stomach local variations in pepsin secretion, and instead we use the pepsin activity measured in the body of the stomach as the reference value. This value ranges from 180 to 780 U/mg protein (using hemoglobin as a reference substrate) between individuals.\textsuperscript{44} Pepsin output and total gastric fluid secretory volume output are parallel and proportional processes, so pepsin concentration in gastric juice can be regarded as constant.\textsuperscript{43,54}

### 3.2 Simulation Approach, Reference Values and Uncertainty of the Model’s Intrinsic Parameters

The mechanical movements of the stomach and residence time of food in it are also known to have an impact on food transformation. Kong & Singh\textsuperscript{8} reviewed the state of the art in this field.

For each individual particle, as shown in section 1.2.1, the mass transfer at the gastric fluid–bolus particle interface depends on the Reynolds (Re), Sherwood (Sh) and Schmidt numbers (Sc), hence of the fluid velocity ($v$), fluid dynamic viscosity ($\mu$), fluid density ($\rho$), of the particle size (under the Size = $L_{\text{car assumption}}$) and of the diffusivities ($D$).

Fluid in the stomach has a non-Newtonian behavior.\textsuperscript{55,56} Abrahamsson et al.\textsuperscript{46} suggested that the in vivo fluid flow around 1cm-diameter tablets is laminar with a Reynolds number of an order of 0.01 to 30, and in all cases orders of magnitude below those required for the existence of turbulence.

The flow velocity established by the propagation speed of antrum contraction waves is 2 to 3 mm.s$^{-1}$.\textsuperscript{47,48} The strongest fluid motion is around the lumen occlusion, with a velocity of up to 12 mm.s$^{-1}$ in the narrowest region.\textsuperscript{20}

The dynamic viscosity of the gastric juice in the stomach is in the range 0.01 to 2 Pa.s.\textsuperscript{45}

The density of the gastric fluid is close to that of water.\textsuperscript{45,46}
The diffusivity values used for hydrochloric acid and for pepsin are the values corresponding to their mass diffusivity in water, as we work to the assumption that these chemical compounds diffuse essentially in the aqueous phase of the meat particles.

For the entirety of the solid food bolus, after ingestion, the rate of gastric emptying starts with a lag phase during which there is very little emptying, followed by a linear phase of emptying. The residence time of a piece of solid food in the stomach depends on composition of the meal, size of the piece, and physiological parameters. Residence time in the stomach, mechanical movements, and particles diameters are all inter-connected, since particle size is reduced during digestion. Gastric emptying is generally complete after 2 to 5 hours. In the reference situation used for this study, the lag phase lasts 1h (t_{lag}) and gastric emptying is complete after 4h (t_{end}) (see Fig. 4a and Malagelada et al.).

Particles with a size lower than 1 to 2 mm can pass through the pylorus and hence be emptied from the stomach into the duodenum.

Particle digestion is calculated numerically and locally and then averaged to obtain mean particle gastric digestibility ratio over time (eq. 14) and mean particle gastric digestibility ratio over a gastric emptying period (eq. 15).

The result of the simulations depends on both the factors studied and their physiological variations and on the values of the model’s intrinsic parameters which are known with a degree of uncertainty. We therefore used a hierarchical cluster analysis to confirm that the factors studied were effectively the major factors driving digestion and to have a study on the accuracy of the result linked to the uncertainties in knowledge of the parameter values.

The relative influences of parameters were evaluated using Statistica® (version 13.1). The weight matrix reflecting the covariance structure between the predictor and response variables was produced by partial least squares (PLS) regression. These weights are computed so that each of them maximizes the covariance between the digestibility (response) and the corresponding factor scores. Implementation of the NIPALS algorithm normalizes these weights.

Within the Statistica® PLS module, default settings were chosen. The dependent variable studied is the digestibility parameter $\bar{\sigma}$ while the mass transfer correlation is a categorical predictor, and buffering, gastric pepsin activity, particle size, physiological gastric fluid dynamics parameters and acidification are continuous predictors.

4 RESULTS AND DISCUSSION

Hierarchical clustering confirmed that the two factors investigated in most depth in this paper, i.e. size of the bolus particles and variations in meat pH, are the major factors dictating prediction of the gastric
digestibility of meat. Pepsin content in the stomach does not appear to be a limiting factor. The in-depth study of the result of the hierarchical clustering and the effect of parametric uncertainties on the digestibility values calculated by the model is presented in section 4.3.

4.1 DETERMINATION OF MEAT BUFFERING CAPACITY

Modeling the pH buffering capacity of the meat bolus hinges on two parameters: the mass transfer coefficient $k$ which accounts for transfers between the fluid and the meat surface in our experimental device (Fig. 2), and the parameter describing the pH buffering capacity of the meat $K_H$, which accounts for the effect of the meat particle’s chemical composition on its acidification. $K_H$ is determined primarily based on pH profile measurements in the meat cylinders whereas $k$ is determined on experiments conducted with meat slices completely submerged in the acid solution. The parameter pairs $\{k, K_H\}$ determined have to fit with all the experimental measurements in order to account for both buffering capacity within the product and surface exchange.

Experimentally-measured pH profiles inside thick cylinders show that pH change in the meat remains restricted to within a zone that is less than 10 mm thick, even for the longest experimental running times (Fig. 3a). Observations showed that for the acidification effect to become perceptible at depths of 5, 8 and 10 mm, the experiment had to be left to run for at least 6, 18 and 24h, respectively (Fig. 3a). Furthermore, pH value in the first few tenths of a millimeter in from the surface showed relatively little variation during the first 18 hours of the experiment (Fig. 3a), whereas mean pH value in the 2 mm-thick slice of meat decreased relatively steadily over the 3½h experiment (Fig. 3b).

The $\{k, K_H\}$ parameter pairs have to be able to model the experimental results obtained both on cylinders and slices. The value space for $\{k, K_H\}$ is fairly wide when we only consider the pH profile measured on the cylinders at the 6h trial time point, but it shrinks to an elliptical zone bracketed between the following intervals of variation: $3E-8 \text{ m.s}^{-1} \leq k \leq 9E-9 \text{ m.s}^{-1}$ and $0.014 \leq K_H \leq 0.031$, when also factoring in the profiles obtained after 18h of trials. Adding the pH profiles measured at the 24h trial time point narrows the value space down to just one parameter pair, i.e. $k = 1.0^{±0.2} * 10^{-8} \text{ m.s}^{-1}$ and $K_H = 0.030^{±0.002}$. Note here that this parameter pair leads to calculated pH profiles on meat cylinders that are in very good agreement with the experimental results for distances-to-surface greater than 2 mm and experiment times of 6h and 18h (Fig. 3a). The calculation–measurement fit is not quite as good for local points very near the surface and for the 6h experiment time point (Fig. 3a, experiment run for 6h and measurements performed at less than 2 mm from the meat surface). Furthermore, the values predicted by the model do not match with the experimental measurement points for a 24h trial. These calculation-to-measurement gaps are directly linked to the simplicity of the model used. This is because immersing the meat in a hydrochloric acid solution has the effect of
not only causing protons to migrate to the meat but also causing meat ions to diffuse to the acid solution, which the model fails to predict and which explains the near-surface gaps observed in the pH profiles measured on the cylinder after 6h of immersion. The big gaps observed on the cylinders at the 24h experiment time point are directly linked to acid-driven degradation of the product, which again is not accounted for in the model.

Considering here all of the pH profiles obtained on the cylinders for contact periods ranging from 6h to 24h enabled us to narrow the value space down to just one pair of values for the \(\{k, K_H\}\) parameter set, which accounts for both the effects of proton penetration into the meat and local-point pH variation in the product. Not considering acid-driven product degradation in the model did not affect the rest of the study, since the effects only materialize at experiment times upwards of 18h whereas gastric degradation times are under 5h.\(^{35-38}\)

### 4.2 Simulation of the Effect of Change in Gastric pH Over the Course of Digestion

We used the previous diffusion–buffering mathematical model to predict the time–course change in pH of meat particles in the stomach. The size of the meat particles introduced in the calculations and assumed to remain constant during gastric digestion was either 2mm or 4.25mm: 2 mm reflects the size of particles able to exit the stomach via the pylorus\(^{37}\) and 4.25 mm reflects the median size of particle in the bolus after mastication\(^{5,42}\), which is assumed to remain the same when reaching the stomach. The pH of the meat particles reaching the stomach is also assumed to be equal to the pH of the fresh meat, i.e. pH 5.5 on average.

Fig. 4a charts the time–course change in calculated mean pH inside 4.25 mm-sized meat particles. When the model ignores meat buffering capacity and assumes a gastric pH at a constant 1.5 throughout digestion, meat pH drops to below 2.0 in less than 5 minutes, whereas it takes over 55 minutes as soon as the buffer effect is introduced (see Fig. 4a, curves 1 and 2). In reality, pH of the gastric fluid varies over the course of digestion, and is given here by the curve published by Malagelada et al.\(^{43}\) who observed a peak of gastric pH at approximately pH = 4.7 after meal ingestion followed by a fall to pH < 3.0 after 60 minutes. It takes more than 1½ hours to recover the baseline gastric pH level measured on the fasting subject used in the study (grey points, Fig. 4a). In this case, the pH drop in the meat particles is a lot slower and it takes over 90 min for meat pH to reach 3.0 and 180 min for meat pH to drop below 2.0 (see Fig. 4a, curve 3). In the case where in-stomach acidification is assumed to be more than 0.5 pH units higher (translation of +0.5 pH of the curve of Malagelada) than in Malagelada et al.\(^{43}\) reference curve, meat pH remains higher than 2.0 even after 4 hours of digestion (see Fig. 4a, curve 4).
As pepsin activity is hugely dependent on pH change of the meat and its buffering capacity, these variations have a big impact on percentage of proteins digested.

In the case where gastric pH is at a constant 1.5 from start to finish throughout digestion, the times required to reach a relative digestion $\bar{\sigma}$ of 50% or of 75% compared to maximum myofibrillar digestibility, written $t_{\bar{\sigma}=50\%}$ and $t_{\bar{\sigma}=75\%}$, for the proteins contained in the 4.25mm-diameter meat particles are 1h and over 1½h, respectively (Fig. 4b, curve 1). When pH of the gastrovascular cavity follows Malagelada et al.\textsuperscript{43} reference curve, it takes over 2h10min and 2h50min, respectively, to achieve the same results (Fig. 4b, curve 2). These times were even longer when physiological factors caused the in-stomach pH values drift more than 0.5 pH units from Malagelada et al.\textsuperscript{43} reference curve values, in which case $t_{\bar{\sigma}=50\%}$ and $t_{\bar{\sigma}=75\%}$ were 2h50min and over 3h, respectively (Fig. 4b, curve 3).

In reality, the meat particles decrease in size over the course of digestion and only exits the stomach when they are less than 2.0 mm in diameter. In Fig. 4b, curve 4 simulates the effect of reducing particle diameter from 4.25mm to 2.0mm on protein digestion rate in the case where gastric pH follows the reference curve. The effect of this reduction of particle diameter decreases the $t_{\bar{\sigma}=50\%}$ and $t_{\bar{\sigma}=75\%}$ values by over 30 minutes when gastric pH is given by the reference curve (Fig. 4b, curves 2 and 4).

Thus a meat particle entering the stomach at a size of 4.25mm and decreasing to a size of 2mm would have a digestibility situated in-between the results obtained for D = 4.25mm and D = 2 mm (Fig. 4b, curves 2 and 4).

### 4.3 EFFECT OF BIOLOGICAL VARIABILITY AND PARAMETER UNCERTAINTY ON PREDICTED MEAT DIGESTIBILITY

The relative influence of the different factors and parameters given in Table 1 can be calculated using the PLS procedure described in section 3.2. Results in Fig. 5 show that bolus particle size and gastric pH deviation from Malagelada et al.\textsuperscript{43} reference profile are the most important biological factors, which impact protein digestibility. These two factors are equally important and can combine together. For example, there may be an age-related slowdown in acidification capacity in the stomach together with an age-related loss of masticatory efficiency that increases particle size in the food bolus. Peristaltic movements have far less influence that these factors, whereas gastric pepsin-related variation has only a minor effect in the concentration and activity range considered here. The uncertainty over the correlations and parameters to introduce in the model has a statistically significant effect on the results, but is still not high enough to undermine the conclusions on the effect of particle size and buffering capacity and the variation in gastric pH on meat protein digestibility.

### 4.4 PROTEIN DIGESTIBILITY AT THE END OF GASTRIC DIGESTION
In Table 1, the most probable conditions are flagged with superscript o whereas the favorable extremes are flagged with superscript + and the unfavorable extremes are flagged with superscript -. As the choice of correlation for the surface mass transfer coefficient is a categorical parameter that can take only two levels, we have opted to use the mean of the digestibilities obtained for the two correlations for the average case. Table 2 gives the change in digestibility as a function of particle size and pH gap to the physiological reference curve. Meat protein digestibility following particle residence time in the stomach is computed from eq. 15, accounting for the reference curve and potential gaps to physiological pH. The cumulative impact of potentially viable variations on the physiological factors and the intrinsic model parameters can also serve to define the upper and lower bounds of this digestibility index, by considering the most favorable and least favorable extreme conditions (reported in ± format in Table 2).

The results of the simulations in Table 2 tell us that the in-stomach relative digestion $\bar{\sigma}$ of proteins contained in the meat particles decreases quasi-linearly as a function of both particle diameter and decline in stomach acidification compared to the reference curve. The relative loss of digestibility related to these two factors grows stronger as gastric conditions grow more limiting. Protein digestibility index $\bar{\sigma}$ reaches 77% on exit from the stomach in the most favorable conditions, i.e. for 0.5mm-diameter particles following the reference pH curve, but falls to just 41% either when particle diameter increases up to 6mm or when gastric pH deviates by one pH unit from Malagelada et al. reference curve (i.e. variation along the second column and the first row of Table 2, respectively). These two effects can compound to drive in-stomach protein digestibility down to practically zero.

The superscript values that account for the parameters connected with gastric mobility, via the mass transfer coefficient, have a substantially smaller effect than the parameters related to particle size or to variation in gastric pH value, and can even be considered negligible in the case of a very small initial particle size, where pepsin and proton diffusion will be fast regardless of particle movement in the stomach, but not in the case of bigger particle size, where a very low transfer coefficient can reduce protein digestibility $\bar{\sigma}$ to practically zero. As indicated in the last row of Table 2, the calculated differences in digestibility values between a mobile particle and an immobile particle can be about as big as the digestibility value itself (i.e. 41%–34% in the last row of the first column of Table 2, and 4%–4% in the last row of the last column of Table 2).

Physiologically speaking, these factors all pull in the same direction. Advancing age tends to bring about a decline in masticatory capacity, hydrochloric acid secretion, and gastric motor function. Results of model output prove that these 3 effects are synergistic and can cause gastric protein digestibility to collapse from around 75% to 0%. However, the very low digestibility thus obtained is underestimated
due to the particles in the liquid phase of the food bolus that are not included in these estimates and yet contribute to dietary protein supply. The digestibility of these very small particles is not diffusion-limited and would therefore be higher, provided that the particles reside long enough in the stomach to make contact with the active pepsin.

In vivo experiments have proved that the utilization of meat for protein synthesis can be impaired by a decrease in the chewing efficiency of elderly subjects and that for elderly persons protein assimilation could be affected by meat cooking conditions. On the contrary In vitro experiments performed in a TIM gastro-intestinal system seemed to conclude that age has little effect on the digestibility of meat proteins. However during these experiments ageing was only taken into account by a difference in the gastric acidification rate without considering the pH fasting value or the size of the bolus particles entering the stomach. The present modeling work bring complementary quantitative data which tend to prove that chewing and acidification problems can combine to decrease sharply the digestibility of proteins at the outlet of the stomach; this difference of digestibility being connected to the lack of assimilation of meat proteins by the elderly. Indeed, if the nature and the concentration of the peptides hydrolyzed at the entrance of the duodenum are determinant to limit muscle mass loss linked with sarcopenia as suggested by Boirie & Guillet, then the present model can be helpful to design new dietary strategies to decrease these detrimental effects in the elderly populations.

CONCLUSION

To the best of our knowledge, this work marks the first attempt to quantify the processes involved in gastric digestion of meat using a combined reaction–diffusion model. The reaction–diffusion model developed in this paper is able to provide quantitative data on the gastric digestion of meat proteins by pepsin, much of which would be hugely time-intensive if not impossible to obtain experimentally. The study shows that size of bolus particles and change in gastric pH have an overriding effect on the percentage of protein digested in the stomach and that the pH buffering capacity of the meat has to be accounted for to properly calculate the gastric digestibility of meat as soon as the bolus particle is a few millimeters large.

From a nutritional standpoint, the model developed here clearly shows the consumer age factor, as masticatory capacity and hydrochloric acid secretion tend to decrease and gastric motor function tends to get weaker with advancing age which could, in extreme cases, lead to a near-zero digestibility value. This age-related loss is further compounded by the fact that passage through the stomach is just one step—and one that occurs relatively quickly compared to the total time of end-to-end transit through the digestive system from preparation through to absorption in the small bowel. High in-stomach
digestibility thus promotes a swift increase in amino acid concentration in the blood and consequently stimulates protein synthesis, which could offer a nutritional strategy to counter sarcopenia.

Even though the model provides undeniably valuable insights to help understand declining protein digestion in the stomach of older people, it still has room for improvement, especially in the way it accounts for the time–course change in particle size. Our model can be rapidly improved to take into account the progressive reduction of the particle size in the stomach connected to its digestion, while its possible breakdown into smaller particles would be more complex to describe mathematically. This would require coupling with a disintegration kinetics model for meat particles, similarly to the one developed for carrot and ham. Moreover this breakdown would have to be connected with particle movement which was only accounted for in the paper indirectly via the mass transfer coefficient at the meat particle–gastric fluid interface. Likewise, our approach considers the change in gastric pH as a model input taken from the literature, whereas in reality, hydrochloric acid and pepsin secretions occur concomitantly with successive filling and emptying of the stomach, and the variation in gastric pH could be predicted from these processes and from the volume of all the foods ingested in a meal and their respective buffering capacity. The gastric emptying rate, also taken from literature in this approach, could also be related to particles sizes. This mass transfer–reaction model could thus be profitably complemented with models of fluid mechanics and buffering capacity in the stomach, which would pave the way to predicting the complete cycle of all these processes together.

**Conflicts of interest:** There are no conflicts of interest to declare.

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**Table 1**: List of (1) the main factors needed to calculate the effect of the physiological phenomena on protein digestibility and their potential range of variation, and (2) the intrinsic parameters introduced in the model, their most probable value and their range of uncertainty. In a list of values, the most probable value is indicated by the o superscript while the extremes most and least favorable digestion conditions used in the calculations are indicated by + and – superscripts, respectively.

| Processes                          | Parameters                        | Value spaces studied                                                                 | Source |
|-----------------------------------|-----------------------------------|--------------------------------------------------------------------------------------|--------|
| (1) Main factors studied          |                                   |                                                                                      |        |
| Mastication                       | Particle size (diameter)          | \{ 0.5, 1, 2, 3.5, 5, 6 \} mm                                                      | 5, 42  |
| Gastric acidification             | Reference pH profile with potential physiological gap                                | Baseline pH between 1.3 and 2.1—healthy subjects Baseline pH up to 2.9—sick patients | 43     |
| Variation in enzymatic activity   | Gastric pepsin activity           | \{ 180°, 330°, 480°, 630°, 780° \} U/mg of proteins (using hemoglobin as substrate) | 44     |
| Variation in pH of meat particles | Buffering capacity, \( K_H \)      | \{ 0.014°, 0.030°, 0.031° \}                                                       | Experiment (§2 and §4.1) |
| In stomach mobility of meat particles accounted for via the value of the convective transfer coefficient, \( k \) | Type of correlation used for determining \( k \) and \( k_{\text{pepsin}} \) | Forced convection around a solid sphere or wall-to-fluid mass transfer in liquid–solid fluidized beds | 33, 34 |
| Physiological gastric fluid data used in the correlation | Dynamic viscosity, \( \mu \) | \{ 0.01°, 0.3°, 2° \} Pa.s | 45 |
| | Reynolds number, \( Re \)  | \{ 0.1°, 2°, 30° \} | 46 |
| | Velocity, \( v \) | \{ 0.5°, 2.5°, 12° \} \( \text{mm.s}^{-1} \) | 47, 48, 20 |
| (2) Intrinsic model parameters    | Diffusivity, \( D_{\text{pepsin}} \)         | 1.4E-10 \( m^2.s^{-1} \)                                                        | 49     |
| Acid diffusion                    | Diffusivity, \( D_{\text{HCl}} \)         | 3.3E-9 \( m^2.s^{-1} \)                                                        | 33     |
| Pepsin-driven protein degradation | pseudo rate constant of reaction \( L \) | 2.45 ± 0.69                                                                       | 24     |
| | log10 of kinetic rate constant of the absorption reaction on cleavage sites \( pK\alpha_1 \) | 1.6 ± 0.2                                                                       |        |
| | log10 of kinetic rate constant of the desorption reaction on cleavage sites \( pK\alpha_2 \) | 2.5 ± 0.3                                                                       |        |
| Gastric residence time            | \( t_{\text{lag}} \) | 1h                                                                                   | 43     |
| | \( t_{\text{end}} \) | 4h                                                                                   |        |
Table 2: Average value of $\bar{\sigma}$ at the end of gastric digestion for increasing radius of the meat particles and pH deviations (a positive deviation is an upwards translation) from the reference curve of Malagelada & al.\textsuperscript{43}. Upper and lower bounds in the superscripts account for the most or conversely the least favorable digestion conditions (indicated by superscripts + and – in table 1), connected with pepsin activity, gastric dynamic behavior and meat buffering capacity. The column in bold gives the results obtained for the reference gastric pH evolution of Malagelada & al.\textsuperscript{43}.

| Particle size (mm) | Healthy fasted pH range | Abnormal fasted pH |
|-------------------|-------------------------|--------------------|
|                   | Difference in gastric pH to physiological reference |
|                   | -0.2 | 0   | 0.2 | 0.4 | 0.6 | 0.8 | 1  | 1.2 | 1.4 |
| 0.5               | 75\textsuperscript{+10}_{-4} | 77\textsuperscript{+0}_{-5} | 76\textsuperscript{+0}_{-6} | 72\textsuperscript{+0}_{-7} | 64\textsuperscript{+0}_{-8} | 53\textsuperscript{+0}_{-7} | 41\textsuperscript{+1}_{-6} | 31\textsuperscript{+0}_{-6} | 21\textsuperscript{+0}_{-4} |
| 1                 | 74\textsuperscript{+0}_{-8} | 75\textsuperscript{+1}_{-12} | 74\textsuperscript{+1}_{-16} | 70\textsuperscript{+1}_{-20} | 61\textsuperscript{+2}_{-20} | 51\textsuperscript{+1}_{-20} | 39\textsuperscript{+1}_{-16} | 29\textsuperscript{+1}_{-13} | 20\textsuperscript{+1}_{-10} |
| 2                 | 70\textsuperscript{+2}_{-21} | 70\textsuperscript{+2}_{-29} | 67\textsuperscript{+3}_{-34} | 62\textsuperscript{+3}_{-37} | 53\textsuperscript{+4}_{-35} | 43\textsuperscript{+3}_{-31} | 33\textsuperscript{+3}_{-25} | 24\textsuperscript{+2}_{-19} | 16\textsuperscript{+2}_{-13} |
| 3.5               | 62\textsuperscript{+4}_{-40} | 59\textsuperscript{+5}_{-42} | 54\textsuperscript{+6}_{-42} | 46\textsuperscript{+7}_{-38} | 38\textsuperscript{+6}_{-33} | 29\textsuperscript{+6}_{-26} | 21\textsuperscript{+5}_{-19} | 15\textsuperscript{+4}_{-14} | 10\textsuperscript{+3}_{-9} |
| 5                 | 50\textsuperscript{+5}_{-39} | 45\textsuperscript{+7}_{-37} | 39\textsuperscript{+8}_{-34} | 32\textsuperscript{+8}_{-29} | 25\textsuperscript{+7}_{-23} | 18\textsuperscript{+6}_{-17} | 13\textsuperscript{+5}_{-12} | 9\textsuperscript{+3}_{-9} | 6\textsuperscript{+2}_{-6} |
| 6                 | 41\textsuperscript{+0}_{-34} | 36\textsuperscript{+1}_{-31} | 30\textsuperscript{+0}_{-27} | 24\textsuperscript{+0}_{-22} | 19\textsuperscript{+7}_{-18} | 14\textsuperscript{+5}_{-13} | 10\textsuperscript{+4}_{-10} | 7\textsuperscript{+3}_{-7} | 4\textsuperscript{+3}_{-4} |
**Solid bolus of unlinked spherical** meat particles of different sizes $\geq 0.5\text{mm}$ and $\text{pH} = 5.5$

**Figure 1:** General description of the mathematical model and assumptions
Figure 2: Experimental setup for meat acidification measurement
Figure 3: (a) pH profile measured in the first cm of the central portion of meat cylinders after different experimental times: 6h (black, diamonds), 18h (orange, squares) and 24h (blue, circles), experimental mean points are linked by dashed lines. Solid lines are model predictions with $k = 1E-8$ m.s$^{-1}$ and $K_H = 0.030$ for the following time periods: 6h (black), 18h (orange), 24h (blue). (b) Time-course change in average pH in 2mm-thick meat slices immersed in acid solution (experiments: squares; simulation: solid line); (a, b) Experimental points represent mean values while errors bars represent ± 2 * standard deviations calculated on 3 repetitions. All unspecified model parameters are set at their reference value during these simulations, flagged with a superscript ° in Table 1.
**Figure 4(a):** Average pH change of a 4.25mm-diameter meat particle. The grey square points with error bars show change in reference gastric pH measured by Malagelada & al.43 The 4 other curves are the calculated average pH of the particle. Unspecified model’s parameters have been set at their reference value (superscript ° in Table 1). Simulations were performed: 1 (semi-dotted): with a constant gastric pH of 1.5 and without meat pH buffering, 2 (dashed): with a constant gastric pH of 1.5 and considering
meat pH buffering, 3 (solid with error bars): with a reference gastric pH following the curve of Malagelada et al.\textsuperscript{43} (with errors bars showing the uncertainty propagation induced by the error bars on reference gastric change) and meat pH buffering, 4 (dotted): with addition of +0.5 pH units to the gastric pH curve of Malagelada et al.\textsuperscript{43} (upwards translation) and meat pH buffering.

**Figure 4(b):** Effect of particle size and gastric pH. Meat buffering is always included in these simulations. All unspecified parameters of the model are set at their reference value (superscript * in Table 1). Simulations of the digestibility index $\sigma(t)$ were performed: 1 (black dashed): with a constant gastric pH of 1.5 and 4.25mm-diameter meat particle, 2 (black solid with error bars): with a reference gastric pH following the curve of Malagelada et al.\textsuperscript{43} and 4.25mm-diameter meat particle, 3 (black dotted): with addition of +0.5 pH units to the gastric pH curve of Malagelada et al.\textsuperscript{43} (upwards translation) and 4.25mm-diameter meat particle, 4 (grey solid with error bars): with a reference gastric pH following the curve of Malagelada et al.\textsuperscript{43} and 2mm-diameter meat particle.
**Figure 5**: Impact of factors and uncertainties on meat protein digestibility.
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