X-RAY BINARIES AND THE CURRENT DYNAMICAL STATES OF GALACTIC GLOBULAR CLUSTERS

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ABSTRACT

It has been known for over 30 years that Galactic globular clusters (GCs) are overabundant by orders of magnitude in bright X-ray sources per unit mass relative to the disk population. Recently a quantitative understanding of this phenomenon has developed, with a clear correlation between the number of X-ray sources in a cluster, \( N_X \), and the cluster’s encounter frequency, \( \Gamma \), becoming apparent. We derive a refined version of \( \Gamma \) that incorporates the finite lifetime of X-ray sources and the dynamical evolution of clusters. With it we find we are able to explain the few clusters that lie off the \( N_X-\Gamma \) correlation, and resolve the discrepancy between observed GC core radii and the values predicted by theory. Our results suggest that most GCs are still in the process of core contraction and have not yet reached the thermal equilibrium phase driven by binary scattering interactions.

Subject headings: globular clusters: general — methods: numerical — stellar dynamics

1. X-RAY SOURCES AND CLUSTER DYNAMICS

It was realized more than 30 years ago that Galactic globular clusters (GCs) are overabundant by orders of magnitude in bright X-ray sources per unit mass relative to the disk population \cite{Clark1975, Katz1975}. It was quickly understood that strong dynamical scattering interactions of binaries in the dense cluster cores should be responsible for this overabundance \cite{Verbunt1987}. With the advances in X-ray astronomy made possible by observatories such as Chandra, the relationship between X-ray sources and core cluster dynamics has recently been quantitatively studied. Pooley et al. \cite{Pooley2003} performed Chandra observations of many Galactic GCs down to a limiting luminosity of \( 4 \times 10^{30} \text{ erg/s} \) in the 0.5–6 keV range (which includes low-mass X-ray binaries [LMXBs] in outburst and quiescence, cataclysmic variables [CVs], millisecond pulsars [MSPs], and magnetically active main sequence binaries [ABs]), and looked for correlations between the number of X-ray sources in each cluster and properties of the cluster itself. They found the strongest correlation with the “encounter frequency” \( \Gamma \), a rough estimate of the current dynamical encounter rate in the cluster. More recently, Heinke et al. \cite{Heinke2003} and Pooley & Hut \cite{Pooley2006} have isolated the quiescent LMXBs (qLMXBs) and CVs, respectively, from the X-ray source populations, and have shown that their numbers are indeed consistent with dynamical formation.

These results represent quantitative, empirical evidence that dynamical encounters are responsible for the formation of X-ray sources in clusters. However, they suffer from at least a few drawbacks. First, the correlation between the number of X-ray sources, \( N_X \), and the encounter frequency appears to be sub-linear, with \( N_X \propto \Gamma^{0.74 \pm 0.36} \), although for LMXBs the exponent is \( 0.97 \pm 0.5 \) \cite{Pooley2003}. Second, there are three clusters for which \( N_X \) is significantly larger than predicted by \( \Gamma \). In the original work of Pooley et al. \cite{Pooley2003} it was already clear that NGC 6397 has an \( N_X \) that is \( \sim 5 \) times larger than predicted by the \( N_X-\Gamma \) correlation.

Recent observations show that \( N_X \) is factor of \( \sim 2 \) times that predicted by \( \Gamma \) for NGC 7099 \cite{Lugger2007}, and a factor of \( \sim 20 \) for Ter 1 \cite{Cackett2006}. The \( N_X \) error bars for Ter 1, NGC 6397, and NGC 7099 represent source counting noise and background source uncertainty, but for the remaining clusters represent only background uncertainty.

2. UNDERSTANDING CLUSTER CORE RADIUS

The evolution of a GC, being a bound self-gravitating system, is very similar to the evolution of a star, and comprises three main phases. In the “core-contraction phase,” the first phase of evolution, the cluster’s core

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contracts on a relaxation timescale, much like a pre-main sequence star. Once the core density becomes large enough for binary stars to begin strongly interacting dynamically, and thus generating energy via super-elastic encounters, the cluster settles into the “binary-burning phase,” analogous to the main sequence in stars. In this phase the dynamical properties of the cluster core remain roughly constant (e.g., Gao et al. 1991; Heggie & Hut 2003; Fregeau & Rasio 2007). Once the binary population is exhausted in the cluster core, it will collapse via the gravothermal instability, leading to extremely high central densities. Deep in collapse, an energy producing event, such as an interaction of a dynamically-formed binary, will reverse the collapse, causing the core to rebound and enter the “gravothermal oscillation phase,” in which the core continues to collapse and rebound (Heggie & Hut 2003). For a graphical representation of the three main phases of cluster evolution, see Figure 1 of Gao et al. (1991), Figure 5 of Fregeau et al. (2003), or Figure 29.1 of Heggie & Hut (2003).

Since there is strong observational evidence that Galactic GCs were born with significant binary fractions (Hut et al. 1992), and since the binary-burning phase is the longest-lived phase of cluster evolution (perhaps tens of Hubble times; Gao et al. 1991; Heggie & Hut 2003; Fregeau & Rasio 2003; Trenti et al. 2007), it is widely believed that most clusters observed today should be in this phase. Early approximate calculations suggested that the ratio of core to half-mass radius, $r_c/r_h$, in the binary burning phase, is broadly consistent with observations of the $\sim 80\%$ of Galactic GCs that are not observationally core-collapsed (Gao et al. 1991; Fregeau et al. 2003). Recently, however, more accurate simulations have shown that the early calculations overestimate $r_c/r_h$ by a factor of 10 or more (Heggie et al. 2006; Fregeau & Rasio 2007). These latest results are quite difficult to ignore, since they represent the concordance of two completely independent cluster evolution codes—one direct N-body, with minimal approximations and a natural inclusion of binary interactions; the other the approximate Hénon Monte Carlo method, with direct few-body integration of binary interactions. The values of $r_c/r_h$ in the binary-burning phase agree quite well between the two codes, and furthermore agree quite well with semi-analytical theory (Vesperini & Chernoff 1994). The result is that now only the core-collapsed clusters agree with the predicted values of $r_c/r_h$ in the binary-burning phase, implying that if most clusters are in this phase some other energy generation mechanism is responsible for the measured core sizes. Several suggestions have been put forth for the energy source, including, most notably, central intermediate-mass black holes (IMBHs) (Trenti 2006).

One key feature of the evolution of GCs that has escaped careful attention, though, is the timescale of the initial phase of core contraction. Many numerical simulations have shown that it is of order $\sim 10$ initial half-mass relaxation times (Gao et al. 1991; Giersz & Spurzem 2003; Heggie et al. 2006; Fregeau & Rasio 2007). Since the current half-mass relaxation time for most clusters is $\sim 1$ Gyr and was likely much longer in the past, the core contraction phase may easily last longer than a Hubble time (e.g., Hurley 2007). In fact, recent N-body simulations have shown that for a range of initial binary fractions, the evolution of $r_c/r_h$ over a Hubble time is a simple core contraction with no evidence of a binary-burning phase being reached (Hurley 2007). Thus the solution to the discrepancy between theory and observations in $r_c/r_h$ could be the most mundane one, namely that core-collapsed clusters are in the binary-burning phase while the rest are still undergoing core contraction.

3. A REFINED $\Gamma$

First introduced by Verbunt & Hut (1987), the encounter frequency $\Gamma$ is an estimate of the current dynamical interaction rate in the cluster, which is assumed to be proportional to the current number of observable X-ray sources. We refine this predictive quantity by including, among other factors, the recent history of the evolution of the core properties. We start with the general form of the interaction rate, then specialize to the Verbunt & Hut (1987) $\Gamma$, and our new version.

The interaction rate between two species of objects can be written generally as

$$\Gamma \equiv \frac{dN_{\text{int}}}{dt} = \int n_i n_2 \sigma_{12} |\mathbf{v}_{12}| f(\mathbf{v}_{12}) d^3\mathbf{v}_{12} d^3r,$$

where $n_i$ is the number density of species $i$, $\sigma_{12}$ is the interaction cross section between the two species, $\mathbf{v}_{12}$ is their relative speed with $f$ its distribution function, and the integral is carried out over relative velocity space and volume. For the dynamical creation of LMXBs, species 1 represents stellar binaries, while species 2 represents neutron stars. The dynamical formation of CVs and other low-luminosity X-ray sources is rather more complicated, so species 1 and 2 generally represent single and binary star systems (see, e.g., Figure 7 of Ivanova et al. 2006). Typically, the integral in eq. (1) is approximated as

$$\frac{dN_{\text{int}}}{dt} \propto \rho_c^3 v_r^3,$$

where $\rho_c$ is the core mass density, $v_r$ is the core velocity dispersion, the integral has been approximated by the core value, the gravitational-focusing dominated cross section has been used, and $\rho_{c1}/\rho_{c2}$ is assumed to be constant for all clusters. Additionally, it should be pointed out that only the proportionality in eq. (1) has been preserved since several factors (some of which are not constant among clusters) have been dropped. More accurate approximations of eq. (1) have been used, including numerical integrals over cluster models (Pooley et al. 2003), but all are estimates of the current interaction rate.

Dynamically formed X-ray binaries (XRBs) are known to have finite detectable lifetimes. For LMXBs, this lifetime varies from $\sim 10^5$–$10^7$ yr for red giant donors, to $\sim 1$ Gyr for main-sequence companions, to a few Gyr for ultracompacts (Ivanova et al. 2007). For CVs, this lifetime is $\sim 1$ Gyr (N. Ivanova, priv. comm.). An additional complication is that dynamically formed XRBs do not necessarily turn on as X-ray sources immediately following a strong interaction. In fact, the interaction that places a binary on the path to becoming an observable X-ray source typically occurs several Gyr before it becomes detectable (Ivanova et al. 2006, 2007).

Since the XRBs we see now formed a few Gyr or more ago, and since the recent dynamical history of clusters may have been quite variable, it is clear that the current number of observable sources should be proportional to
the interaction rate integrated over time. We thus write
\[ \Gamma \equiv N_{\text{int}} = \int \int \int n_1 n_2 \sigma_{12} |v_{12}| f(v_{12}) d^3v_{12} d^3r dt. \tag{3} \]

We perform the time integration over an interval \( t_x \), the typical detectable lifetime of an XRB, to a time \( t_\ell \), the typical timescale between strong interaction and observability, in the past. We leave \( t_x \) and \( t_\ell \) as parameters, but take \( t_x = 1 \) Gyr and \( t_\ell = 3 \) Gyr as canonical values. We further simplify the integral by writing
\[ N_{\text{int}} = \int_{t_0}^{t_\ell} f_b f_{co} n_c^2 \sigma_{\text{strong}} \sqrt{2} v_\sigma \frac{4\pi}{3} r_c^3 dt, \tag{4} \]
with \( f_b \) the core binary fraction, \( f_{co} \) the core compact object fraction, \( n_c \) the core number density, \( r_c \) the core radius, \( v_\sigma \) the 1-D core velocity dispersion, and \( \sigma_{\text{strong}} \) the cross section for a strong interaction between a binary and a single star. The factor of \( \sqrt{2} \) is from taking the difference of two Maxwellian velocity distributions. The cross section is \( \sigma_{\text{strong}} \sim \pi a^2 G M / (\sqrt{2} v_\sigma^2) \), where \( a \) is the typical semi-major axis of a binary, \( M = 3 m \) is the total mass of the binary–single system, and \( m \) is the typical stellar mass. Taking \( f_b \) and \( f_{co} \) to be constant over the time integral and substituting the definition of the core radius, \( r_c^2 = 9 v_\sigma^2 / 4 \pi G m n_c \) (Heggie & Hut 2003), yields
\[ N_{\text{int}} = f_b f_{co} \frac{81 \sqrt{2} a}{4 \pi G m} \int_{t_0}^{t_\ell} v_\sigma^3 r_c^{-1} dt. \tag{5} \]

This expression is similar to eq. (2), but with the core properties integrated over time. We have kept all numerical factors for the sake of completeness—only the proportionality represented by this equation is needed for what follows. By substituting in for the time evolution of the core quantities in the integrand, one can use this expression to differentiate among the three different phases of cluster evolution. We exclude the gravothermal oscillation phase, since in this phase a cluster should have no more than a few binaries in its core, and all clusters considered here with measured core binary fractions show evidence for many more binaries than this (that a recent estimate puts the core binary fraction of NGC 6397 at 15 ± 1%; Davis & Richer 2004). In the binary-burning phase the core radius and velocity dispersion are constant, so the integral is easy to evaluate. For the core contraction phase, we adopt the time evolution of the core radius shown in the N-body models of Hurley (2007), approximated as \( r_c(t) = r_{c,0}(10 - 9t/t_0) \), with \( r_{c,0} \) the current core radius and \( t_0 \) the current cluster age. Since there is essentially no core energy support in the core contraction phase, for the relationship between core radius and central velocity dispersion we adopt the self-similar collapse model, with \( v_\sigma^2 \propto r_c^{-2} \) (Binney & Tremaine 1987). The ratio of the number of interactions for a cluster in the binary-burning phase to the same cluster in core contraction is then
\[ \frac{N_{\text{int,bb}}}{N_{\text{int,cc}}} = \frac{t_\ell}{t_0} \frac{2.835}{(t_0 + 0.315) - (t_0 + 99t_0 + 0.315)^{0.315}}, \tag{6} \]
which has a minimum of 2.0 and a maximum of 17.8 in the range \( t_x = 10^{-4} \)–3 Gyr, \( t_\ell = 10^{-1} \)–10 Gyr, for \( t_0 = 13 \) Gyr. For the canonical values of \( t_x = 1 \) Gyr and \( t_\ell = 3 \) Gyr with \( t_0 = 13 \) Gyr, the value is 5.0. Since the number of X-ray sources should scale roughly linearly with the number of interactions, this suggests that if a cluster is in the binary-burning phase (and has been for a time \( t_x + t_\ell \) to the present), it should have ~5 times as many X-ray sources than it would if it were in the core contraction phase. (If the Pooley et al. (2003) exponent of 0.74 is adopted this factor is 3.3.) Interestingly, the three clusters in Figure 1 that are observed to be core collapsed are the three that have a significantly larger \( N_X \) than predicted by the standard \( N_X - \Gamma \) correlation, by a factor of ~2 to ~20. NGC 6397 has an overabundance factor of ~2, NGC 7099 a factor of ~5, and Ter 1 a factor of ~20. However, we note that the estimate of \( \Gamma \) for Ter 1 is more uncertain than the rest since it comes directly from eq. (2) and not an integral over the cluster profile, and since the velocity dispersion is only estimated as it has not been measured observationally. The similarity between the observed overabundances and those predicted by our simple revision of \( \Gamma \) suggests that the observationally core-collapsed clusters are indeed in the binary-burning phase, while the rest are still in the process of core contraction.

A natural objection to this conclusion is that cluster metallicity may explain the X-ray source overabundance. Studies of bright LMXBs associated with star clusters in external galaxies have shown a strong correlation between cluster metallicity and LMXB incidence, with metal-rich clusters being much more likely to harbor an LMXB (by a factor of 3 or more; Jordan et al. 2004; Sivakoff et al. 2007). However, this result appears to hold only for bright LMXBs. When looking at the low-luminosity LMXB and CV populations in our Galaxy (which comprise the majority of sources in Figure 1), a correlation between source incidence and cluster metallicity is not clearly apparent (Heinke et al. 2007). In any case, the metallicities of the three overabundant clusters are not significantly larger than those of the other clusters in Figure 1 with [Fe/H] values of -1.30, -1.95, -2.12 for Ter 1, NGC 6397, and NGC 7099, respectively, with the rest of the clusters ranging in value from -0.34 (NGC 6440) to -1.75 (NGC 6093) (Harris 1996).

Another possibility is that the XRBs in the low-\( \Gamma \) clusters may be primarily primordial, in which case their number should scale with cluster mass. However, were this the case, a look at cluster absolute magnitudes shows that NGC 6121 would have roughly as many sources as NGC 7099 and more than NGC 6397 and Ter 1, and NGC 6366 would have more than Ter 1 (Harris 1990).

4. DISCUSSION

This letter presents the confluence of three suggestive observational and theoretical results into a self-consistent picture. The first is that of the clusters that have been observed sufficiently to determine their XRB population, the three that are core-collapsed are the same three that have a significant X-ray source overabundance (of a factor of ~2 to ~20). The second is the semi-analytical result derived in this letter that a cluster in the binary burning phase for the last few Gyr should have ~5 times more dynamically formed X-ray sources than if it were in the core contraction phase for the same time. The third is the recently confirmed discrepancy between observations and theory for the core radii of Galactic GCs, which sug-
gests that only the observationally core-collapsed clusters are in the binary-burning phase. In light of these facts, the conclusion that seems very strongly suggested is that most Galactic GCs are currently still in the core contraction phase, while only the ~20% of clusters that are core-collapsed are in the binary burning phase. This goes counter to the widely held belief that most clusters are currently in the binary burning phase, and complicates the many existing studies that have assumed cluster core properties that are constant with time.

The implications of this result are manifold. There are many studies of the dynamical production of interesting source populations in clusters which assume core properties that are constant with time. These include predictions of the formation of blue stragglers (e.g., Mapelli et al. 2004), the evolution of the core binary fraction (Ivanova et al. 2005), and tidal-capture binaries (e.g., Di Stefano & Rappaport 1994), among others. Revising the results may be as simple as scaling predicted source numbers, but may not be so simple for other quantities.

Studies of GC evolution have shown that clusters starting from very different initial conditions evolve toward a common range of values in many observable structural parameters in the binary-burning phase, including the concentration and ratio of core to half-mass radius (Fregeau et al. 2003, Heggie et al. 2006, Fregeau & Rasio 2007). Since most clusters may not be in the binary-burning phase after all, their observed properties are likely to be more strongly correlated with their initial conditions. This makes modeling of clusters a bit more complicated, but on the other hand allows one to more readily deduce something about the initial properties of clusters.

Perhaps antclimactically, our results suggest that the alternative energy sources recently proposed for supporting GC cores are not required. These include the suggestion of IMBHs in many Galactic GCs (Trenti 2003), enhanced stellar mass loss from stellar evolution of physical collision products (Chatterjee et al. 2007), mass segregation of compact remnants in young clusters (Merritt et al. 2004), or evaporation of the stellar-mass black hole subsystem in young clusters (Mackey et al. 2007).

Although the picture painted in this letter is a suggestive one, there are still several caveats and limitations to our analysis. In the derivation of our refined $\Gamma$ we assume that the core binary fraction and abundance of compact objects are constant over the time of integration. Neither is strictly true, although we expect they will not vary enough to significantly change the overabundance value we derive. We have used only one possible expression for the evolution of the core radius in core contraction. While we expect the general behavior to be very similar to what we have assumed here, more work needs to be done to determine if it is universal. Additionally, our analysis ignores the effect of Galactic tidal stripping on cluster mass, which would make a cluster appear overabundant in X-ray sources, and may be relevant for NGC 6397 (Pooley et al. 2003). On the observational side, there are some uncertainties in evaluating $\Gamma$, which is dependent on quantities that are somewhat difficult to measure for core-collapsed clusters.

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