Small Signal Stability Analysis of Multi-Area Power System

Sumit Kumar

Abstract: This paper focuses on methodologies for calculation and examination of oscillatory security of interconnected power system network against constant disturbances. For instance, voltage soundness, transient dependability and oscillatory behaviors are also the measure of power system stability, which must be evaluated. For that proposed strategies based on proportional integral and fuzzy logic controlling techniques are implemented. The integral controller-based technique provides the zero steady-state error and with adequate damping, time to reach steady state can be reduced, on the cost of oscillation in frequency and tie-line power. On the contrary, fuzzy logic has demonstrated that strategies of computational intelligence can alleviate the quick appraisal of oscillatory solidity with less time to reach steady state. Furthermore, Eigenvalues are constructed for small signal stability analysis, utilizing a parallel variation of Arnoldi technique, reducing the time essential for calculation of vast Multi-Area power frameworks. For exhibit purposes, models have been composed utilizing MATLAB/SIMULINK and with the assistance of the fuzzy logic.

Keywords: Eigenvalues, Proportional Integral (PI), Fuzzy Logic(FL), Transmission System Operator (TSO).

I. INTRODUCTION

Control frameworks of the multiarea system are consistently developing with even bigger limits of power and voltage[1]. Present day control frameworks are of a huge size, extending over a wide area of interconnected systems with various divisions and generating stations. With the ever-growing demand for electricity in every part of the world, power grid and power pools are inevitable. Multi-Area power system architecture is more favourable for the deregulated power industry and distributed generation. With the enormous growth of power system, congestion of the power transportation corridors remains as a challenge, the transmission system operator (TSO) might be forced to put up serious measures so as to reduce the thermal limit capacities as a result of this overloading of the power transmission corridors.

Here, a three-area power system is simulated with Proportional Integral (PI) and Fuzzy Logic (FL) control scheme to enhance the reliability and stability of power system. The proposed model consists of two thermal generators and one gas turbine system for power generation which is having a much faster response. Transients due to constant load change, about 2 to 5% of total load in step form, are imposed [12]. The response of gas turbine and the thermal system will be different for the implemented load variation, as the governor time response is different in both types of systems. Our interest is to curb the frequency oscillations happening due to simulated disturbances, from the nominal frequency [3]-[4].

This is to maintain the power system stability and adequate tie-line power flow to avoid over and under loading of transmission lines. PI controlling technique is used for eliminating the frequency deviation and maintaining the steady state error to zero, likewise limiting the tie-line power variation [8]. Systems response dependent on damping factor, eventually, controls the time response of each area to reach a stable state. On the other hand, fuzzy control strategy has proven itself as a better controlling strategy in terms of reaching steady state and maintaining the stability of the system. Small signal stability analysis based on the eigenvalue is also accomplished in this paper keeping the response of thermal and gas turbine system in mind. More negative eigenvalues would be, system stability will be more which is shown in eigenvalue comparisons of the system without a controller and with PI and FL controller [5].

II. DESIGN AND DEVELOPMENT OF PROPOSED MODEL

A. Three Area System

Power pool frameworks interconnected together as utilities would fundamentally work freely inside their own limits and also satisfying the trades of energy by tie-lines in between areas to avoid violation in the transmission network. It is necessary to maintain the planned exchanges of tie-line control and absorption of load change by every zone to lessen the frequency deviations.

In the three-area power system simulated here, each area is having its governor and turbine system [9]. With every load variation, governor’s flywheel mechanism changes its speed and steam input variation will eventually change the turbine speed. Several controlling strategies have been proposed and implemented. The vital regulator having the capability of bringing down the frequency deviation to its minimum value can be placed within the auxiliary circle [7]. By using the PI controller, the power system is more likely to remain stable, with the fast-acting controller strategy.

By selecting appropriate values of proportional and integral gain the oscillatory nature of the first swing can be managed to add further stability to the system. The same system is further simulated with Fuzzy controller and strategies of computational intelligence have shown better results in terms of oscillatory nature and time to reach steady state. Three territory intertwined frameworks would, in this case, be comprised of three power pools which are merged together [14]-[15]. A number of transmission interconnectors for power flow regulation would be arranged in form of streams and having the ability to make adjustments to the power requirement because of the interconnection made between the control territories [19].
B. Fuzzy Deduction As Applied To Load Frequency Model

The fuzzy derivation is a procedure for acquiring new learning through existing information utilizing fuzzy rationale [10],[11]. The working of the fuzzy system is based upon the 25 rule-based with 5- membership function, where two input signal fuzzification is done as shown below [20]-[23]. The single output is defuzzified by using the weighted average method and implemented in each area of the simulated power system.

Table1: Fuzzy Logic Rule Base

| Error (e) | Change in Error(e*) |
|-----------|---------------------|
|           | in2mf 2 | in2mf 3 | in2mf 4 | in2mf 5 |
| inm f1    | outmf 1 | outmf 2 | outmf 3 | outmf 4 | outmf 5 |
| inm f2    | outmf 6 | outmf 7 | outmf 8 | outmf 9 | outmf 10 |
| inm f3    | outmf 11 | outmf 12 | outmf 13 | outmf 14 | outmf 15 |
| inm f4    | outmf 16 | outmf 17 | outmf 18 | outmf 19 | outmf 20 |
| inm f5    | outmf 21 | outmf 22 | outmf 23 | outmg 24 | outmf 25 |

C. State Space Equation And Model

State space analysis is done to understand the inter-area oscillations. As the simulated system is subjected to small load disturbance, so the ability of power system to remain in synchronism against small disturbances is observed by small signal stability analysis. System instability may arise due to two reasons. Firstly, oscillatory response with high amplitude peak, after introducing disturbance and secondly due to a continuous increase in rotor angle because of insufficient synchronizing torque.

State variables of the simulated power system are \([\Delta X_{G1}, \Delta X_{G2}, \Delta X_{G3}, \Delta P_{G1}, \Delta P_{G2}, \Delta P_{G3}, \Delta f_1, \Delta f_2, \Delta f_3, \Delta f_4, \Delta f_5, \Delta f_6, \Delta f_7, \Delta f_8, \Delta f_9, \Delta f_{10}, \Delta f_{11}, \Delta f_{12}, \Delta f_{13}, \Delta f_{14}, \Delta f_{15}, \Delta f_{16}, \Delta f_{17}, \Delta f_{18}, \Delta f_{19}, \Delta f_{20}, \Delta f_{21}, \Delta f_{22}, \Delta f_{23}, \Delta f_{24}, \Delta f_{25}]. \]

\[\Delta f_2(s) = - \frac{B_2 K_p m_2 (s T_2 + 1)}{K_p (s + K_{f1} m_2 + R_2 s (s T_2 + 1) / (s T_f + 1))} \]

\[\Delta f_3(s) = - \frac{B_3 K_p m_3 (s T_3 + 1)}{K_p (s + K_{f1} m_3 + R_3 s (s T_3 + 1) / (s T_f + 1))} \]

\[
\Delta f_2(s) = \frac{2 \pi T_0}{S} [\Delta f_1(s) - \Delta f_2(s)] \\
\Delta f_3(s) = \frac{2 \pi T_0}{S} [\Delta f_1(s) - \Delta f_3(s)] \\
\Delta f_2(s) = \frac{2 \pi T_0}{S} [\Delta f_2(s) - \Delta f_3(s)] \]

Furthermore, the three-area control system state space equations for Eigenvalue calculation can be developed as follows;

\[\Delta \dot{X}_{E_1} = \frac{1}{\tau_{g1}} [\Delta X_{E_1} + \Delta P_{G1} - \Delta f_1 / R_1] \]

\[\Delta \dot{X}_{E_2} = \frac{1}{\tau_{g2}} [\Delta X_{E_2} + \Delta P_{G2} - \Delta f_2 / R_2] \]

\[\Delta \dot{X}_{E_3} = \frac{1}{\tau_{g3}} [\Delta X_{E_3} + \Delta P_{G3} - \Delta f_3 / R_3] \]

\[\Delta \dot{P}_{G1} = \frac{1}{\tau_{t_1}} [\Delta P_{G1} + \Delta X_{E_1}] \]

\[\Delta \dot{P}_{G2} = \frac{1}{\tau_{t_2}} [\Delta P_{G2} + \Delta X_{E_2}] \]

\[\Delta \dot{P}_{G3} = \frac{1}{\tau_{t_3}} [\Delta P_{G3} + \Delta X_{E_3}] \]

\[\Delta \dot{f}_1 = \frac{1}{\tau_{p1}} [\Delta f_1 + K_{ps} \Delta P_{G1} - K_{ps} \Delta P_{B1} - K_{ps} 1 \Delta P_{T1}] \]

\[\Delta \dot{f}_2 = \frac{1}{\tau_{p2}} [\Delta f_2 + K_{ps} \Delta P_{G2} - K_{ps} \Delta P_{B2} - K_{ps} 2 \Delta P_{T2}] \]

\[\Delta \dot{f}_3 = \frac{1}{\tau_{p3}} [\Delta f_3 + K_{ps} \Delta P_{G3} - K_{ps} \Delta P_{B3} - K_{ps} 3 \Delta P_{T3}] \]

\[\Delta P_{T1} = 2 \pi T_{12} [\Delta f_1 - \Delta f_2] + 2 \pi T_{13} [\Delta f_1 - \Delta f_3] \]

\[\Delta P_{T2} = 2 \pi T_{12} [\Delta f_1 - \Delta f_2] + 2 \pi T_{23} [\Delta f_2 - \Delta f_3] \]

\[\Delta P_{T3} = 2 \pi T_{13} [\Delta f_1 - \Delta f_3] + 2 \pi T_{23} [\Delta f_2 - \Delta f_3] \]

State space model is represented in the form of \( \dot{X} = AX + Bu. \) And their final state space matrix comprising of the main, control and disturbance matrices of a three-area system would be;
D. Eigenvalues Analysis

The linearized power system shown in the matrix form can further be analyzed by eigenvalues. Arnoldi algorithm is used for computing approximations to eigenvalues of a non-Symmetric matrix constructed in a state space model, \( \Delta X = [A]X \). Where X is a state vector and A is represented as a State matrix. By taking the Laplace transform of state equation, new equation in \( s \) domain will be \( s \) satisfies the equation \( s \) is the eigenvalue of State matrix \([A]\). For a system to be stable eigenvalues must be in left-hand side of the imaginary axis, otherwise, the system will be unstable. Eigenvalues of the simulated system are analyzed with PI and the FL implemented in the system, which shows more stability with the Fuzzy controller in the system.

III. MODELING AND SIMULATION

The technique of using simulations in the monitoring, analysis and verification of the results obtained from power system is quite very effective and reliable [2]-[3]. The three-area model depicting a large power pool is simulated and the parameters chosen are illustrated below in Table II and figure 1.

![Simulink main model with fuzzy logic of a three-area power pool.](image)

IV. RESULTS AND DISCUSSIONS

As it is shown in the figure below that no error signal is generated in the power system if no controller is employed, and with PI controller, a steady error signal is generated [29]. While using the fuzzy controller in the same system error signal variation and its dynamics depicts the load variation more precisely, hence providing the better results with the proposed strategy. Moreover, in this simulation result we are able to see that when it comes to power pools which are connected together, due to constant and abrupt fluctuations in the power output, there will be corresponding deviations from their standard values for

| Name  | \( K_p \) | \( T_p \) | \( K_i \) | \( T_i \) | \( H \) | \( P_{DD} \) (MW/Hz) | \( \frac{1}{p} \) |
|-------|--------|--------|--------|--------|------|----------------|----------|
| Area 1 | 1      | 0.08   | 1      | 0.3    | 35   | 1.00           | 125      |
| Area 2 | 1      | 0.08   | 1      | 0.3    | 25   | 0.60           | 10       |
| Area 3 | 1      | 0.08   | 1      | 0.3    | 25   | 0.90           | 2.5      |
both frequencies as well as tie-line power passing through these interconnectors.

**Fig.2. The Error signal generated without a controller, PI and fuzzy controller.**

Implementation of the power frequency regulation is there to ensure that frequency deviations from their acceptable limits are minimized during the slow developing faults or disturbances, and to regulate the exchange of power in these power pools. On the other hand, the application of the electromechanical regulators is so as to bring the response to a steady state in the shortest possible time due to their instantaneous action because of the proportional regulator incorporated in them. This proportional component of the regulator is responsible for the generation of a regulating signal which would be corresponding to the deviation response or error of the power transmission network. It would, therefore, be observed that selection of the right value of $K_p$ in terms of the design of controllers is of great importance in as far as reduction of the steady state error in the controllers may be concerned, and at the same time with increased values of $K_p$ could necessitate a reduction in the time constant as well as damping [16].

**Fig. 3. Frequency variation of three areas with PI controller during transients.**

Frequency variation in all the three areas was analyzed using the simulation process and where it was observed that the system response had to come to a steady state condition after the generation of oscillations by using different controllers. Their oscillations are finally reaching to steady state values because of damping provided by PI controller [18]. By using PI controller system stability and performance has increased without increasing the steady state error.

**Fig. 4. Tie-line power of three areas with PI controller during transients.**

The tie-line power variations of all the three areas is shown in figure 4. After providing the load variation in one area, other two areas would as well continue to face variation in their behaviour while they try to settle down after the occurrence of transients. In this regard, PI controllers would then be employed so as to make system response stable and sustainable during dynamic conditions.

**Fig. 5. Frequency controller during transients.**

In this simulation result we are able to see that when it comes to power pools which are connected together, due to constant and abrupt fluctuations in the power output, in this case taking into consideration the rapid and spontaneous small variations in the load of the three-area control system, there will be a corresponding deviation from their standard values for both frequency as well as tie-line power passing through these interconnectors [23]. Implementation of the power frequency regulation is there to ensure that frequency deviation is maintained within acceptable limits during the slow developing faults or disturbances, and to regulate the exchange of power in these power pools. And therefore, for optimization purposes, a fuzzy logic was employed. Small Signal Stability analysis can be done by using Eigenvalues. An Eigenvalue analysis of the system does provide with a better understanding of small signal stability like rotor angle variation [22],[24]. Tie-Line power control and system behaviour under transient’s conditions in terms of state variables [13]. The below-mentioned values describe the System stability of simulated three area system with and without controllers [5].
By comparing the Eigenvalue of a state variable in case of uncontrolled, PID and fuzzy controller system state, behavioural analysis can be done. It has been analyzed that by using different controllers the Eigenvalues started having more negative real part compared to without controller and values become more negative when the fuzzy controller is being employed. In the Multi-Area system, the behaviour of tie-line power and frequency are important to analyze and after using fuzzy controller stability and damping of oscillations have become fast and overall response of system has improved [17], [21].

V. CONCLUSION AND FUTURE WORK

This research work has mainly investigated on oscillatory nature of Multi-Area system during load disturbance, at the same time providing a comparative solution between PI and Fuzzy logic controller. Small Signal Stability analysis with Eigenvalues is also done to validate the results. With the help of Fuzzy controller, the system has shown better stability and rigidity in terms of frequency and Tie-Line Power Oscillations [20]. Small signal stability analysis of system shows Fuzzy controller will act better against PI controller as far as disturbance is small in nature like load change and slow acting faults.

For the Future improvement, we intend to possibly introduce other optimization techniques such as Genetic Algorithm (GA) or Bacteria Foraging Optimization Algorithm (BFOA) program so that they can help in speeding up the entire process and to change the values of the various parameters present in the power system under investigation [25], [26] and which can be used in coming up with the changes in the load demand. This, therefore, will go a long way in terms of contributing to a reduction in the changes in the frequency and a further reduction to the Tie-Line power and thereby help in maintaining the stability of the system. We may also want to incorporate a programming technique and make comparisons of the values obtained and those with the reference. It is also seen that BFOA technique has quicker convergence characteristics [28]. Most of these optimization techniques serve to be quite useful for obtaining the optimized values of the various parameters as compared to the general hit and trial technique which is extremely tedious and time taking method.

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| State Space Variables | Eigenvalues with without controller | Eigenvalues with PI Controller | Eigenvalues with Fuzzy Controller |
|-----------------------|------------------------------------|--------------------------------|----------------------------------|
| $\Delta V_{k} = v_{k}$ | -20.2374-10.6666j | -0.1474-7.3771j | -0.1489-9.6035j |
| $\Delta n_{k} = n_{k}$ | 20.2374-30.6666j | -0.1474-7.3771j | -0.1489-6.0235j |
| $\Delta P_{k} = P_{k}$ | -35.2542 | -0.6166-6.7821j | -0.3036-6.3331j |
| $\Delta P_{k} = P_{k}$ | 6.8442-6.3886j | -6.7539 | -5.5006 |
| $\Delta P_{k} = P_{k}$ | 5.9109-1.3887j | -3.4887 | -3.1997 |
| $\Delta P_{k} = P_{k}$ | 6.8442-6.3886j | -5.2716 | -0.5031-8.0691j |
| $\Delta P_{k} = P_{k}$ | -9.182 | -9.3752 | -0.5031-8.0691j |
| $\Delta P_{k} = P_{k}$ | -7.4095 | -1.7655-0.3751j | -1.5402 |
| $\Delta P_{k} = P_{k}$ | -1.7744 | -1.7655-0.3751j | -1.3581 |
| $\Delta P_{k} = P_{k}$ | -3.9165 | -1.5551 | -1.6058 |
| $\Delta P_{k} = P_{k}$ | 0.0000 | 0.0000 | 0.0000 |
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