Numerical simulation of gas flow and droplet motion in a wave-plate eliminator of the separator-steam-generator system in the waste-heat-utilisation complex

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Abstract. This paper studied the droplet transport and deposition in the turbulent flow inside a wave-plate eliminator of the waste-heat utilisation complex (WHUC). The Lagrangian discrete particle approach was used to simulate the process of liquid separation from wet steam flow. Two different models for droplet-eddy interaction were tested using data from the available literature. The tested numerical model was used to predict the WHUC performance.

1 Introduction

The droplet transport and deposition in the turbulent flow inside a wave-plate eliminator of the WHUC (Fig. 1) [1] were studied using an Eulerian-Lagrangian computational approach. Flash boiling occurs in the nozzle because of a sharp pressure drop which results in a metastable liquid state. The steam-liquid mixture is sent to the expansion unit and then to the wave-plate eliminator. The temperature and pressure of the water entering the nozzle are \( t_{in} = 257^\circ C \) and \( p_{in} = 10 \) MPa. The pressure of the steam-liquid mixture leaving the expansion unit is approximately \( p_{out} = 1 \) MPa. This paper presents the result of numerical simulation of liquid droplet behaviour in the separator. The information about processes in the nozzle and the operating condition at the inlet of the wave-plate eliminator were obtained using the model presented in [2].

2 Mathematical model

There is presently significant number of works devoted to the theoretical and experimental study of two-phase dispersed flow [3]. The Lagrangian discrete particle approach (LDP-approach) was used in this paper to simulate the process of liquid separation from wet-steam flow in the wave-plate eliminator of the WHUC.

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In the LDP-approach, the continuous-phase flow field is computed using the Reynolds averaged Navier-Stokes equations and discrete-phase droplet motion is obtained from the time integration of Newton’s law. Different modifications of the LDP-approach are available in commercial CFD codes. In this work, the approach realised in the author's CFD code ANES [4] was used. The main features are as follows: droplets have no feedback effect on the carrier gas; there is no heat and mass transfer between the dispersed and continuous phases; there is no droplet-droplet interaction (and, therefore, coalescence); droplets behave as hard spheres; drag is the only force acting on the droplets; there is no droplet-film interaction at the wall; only one droplet-wall interaction is considered—the liquid droplets trapped by the wall.

The dispersion of particles due to turbulence in the continuous phase is simulated using a stochastic tracking model [5]. The instantaneous continuous phase velocity is given by

$$u(x, y, z, t) = \bar{u}(x, y, z) + u'(t)$$

where $\bar{u}(x, y, z)$ – the mean fluid phase velocity which was obtained using one of the models to describe the turbulent transport of momentum (the $k-\omega$ model [6] was used in this paper), $u'(t)$ – the fluctuating continuously phase velocity. Many droplets should be injected in the domain until stationary statistics are achieved.

Components of the fluctuating velocity $u'(t)$ are step functions of time. The basic parameters of the function are amplitude $u_t$ and step width $\Delta t$. Two different models were tested. In the first model, all the values calculated at the start of the droplet-eddy interaction used characteristics of the flow at the particle location and remained constant during the droplet-eddy interaction (model №1). In the second model, all the necessary parameters of the droplet-eddy interaction (amplitude of the function and the eddy interaction time) were “modified” by the local flow characteristics at the particle location (model №2).

Amplitude of the fluctuating continuous-phase velocity is calculated by the equation

$$u_{i,t} = \Lambda_i \cdot u_*, \quad u_* = \sqrt{\frac{2 \cdot k}{3}}, \quad i = 1, 2, 3,$$

where $k$ – turbulent kinetic energy, $\Lambda_i$ – a random number drawn from a normal probability distribution with zero mean and standard deviation equal to unit.

In the model №1, the characteristic scale of fluctuation $u_*$ and $\Lambda_i$ was calculated at the start of the particle-eddy interaction and remained constant. In the model №2, $\Lambda_i$ remained constant, but $u_*$ was updated using $k$ at the droplet location.

The droplet is assumed to interact with the eddy over the smaller ($\Delta t_i$) of the two characteristic times:

1. $\Delta t_{\text{life}}$ – the turbulent eddy lifetime,
2. $\Delta t_{\text{cross}}$ – the eddy crossing time.
The eddy lifetime is given by equation

\[ \Delta t_{\text{eddy}} = 2C_{TE} \frac{k}{\varepsilon}, \]  

(3)

The different value of \( C_{TE} \) is used in the literature. The most commonly used are the following equations

\[ 2C_{TE} = \sqrt{\frac{3}{2}} C_\mu^{3/4} \text{ or } 2C_{TE} = \sqrt{\frac{3}{2}} C_\mu^{1/2}, \]  

(4)

which correspond to \( C_{TE} \) from 0.1 to 0.18 (\( C_\mu \) equals 0.09). In this work, constant \( C_{TE} \) was equal to 0.15. For the \( k-\omega \) models, substitute \( \varepsilon = C_\mu k \omega \) is used.

In the model №1, the interaction time \( \Delta t_i \) is calculated at the start of the droplet-eddy interaction and time before the end of droplet interaction with the current eddy is set at \( t_{\text{end}} = \Delta t_i \). This time is reduced by time step \( t_{\text{end}} = t_{\text{end}} - \Delta t \) at each integration time step. At \( \Delta t_{\text{end}} = 0 \), characteristics of the new eddy are calculated. In our model (model №2), time before the end of particle interaction with the current eddy is modified at each time step:

\[ t_{\text{end,new}} = t_{\text{end,old}} \frac{\Delta t_{i,new}}{\Delta t_{i,old}}, \]  

(5)

where \( \Delta t_{i,new}, \Delta t_{i,old} \) – droplet-eddy interaction time, which are calculated using characteristics of the flow at the new and old droplet locations.

### 3 Validation of mathematical model

The validation analyses are performed through comparison with available experimental data on removal efficiencies of the wave-plate eliminator [7]. Fig. 2 shows comparison results of calculation and experimental data [7].

![Fig. 2. Comparison between the predicted droplet-removal efficiency \( E \) and the experimental data of Ghetti [7] at gas velocities equal to 3 m/s. 1 – experimental data [7], 2 – model №1, 3 – model №2, 4 – without turbulence dispersion.](image)

The calculation results show that the experimental dependence of the efficiency of the separator (the relation of liquid weight at the outlet and at the inlet) from the particle diameter is well reproduced with model №2. However, such a parameter as the cut-off
diameter (a particle diameter at which 95% of particles were trapped at the wall) can be determined without using a turbulent dispersion-particles model. For example, the experimental value of the cut-off diameter for the bulk velocity of continuous-phase flow equals 3 m/s is 8.5 μm, and the value of this parameter is calculated without considering the turbulent dispersion equals to 9 μm.

4 Problem statements and results

The wave-plate eliminator of the WHUC is a cylindrical channel with an inner diameter of $D_{sep} = 85$ mm, in which several zig-zag plates are installed. At the inlet, wet steam has a flow rate of $G_0 = 0.317$ kg/s and a vapor mass fraction of $x = 0.139$ at $p_{out} = 1044$ kPa (it corresponds to $t_{in} = 257$ °C and $p_{in} = 10$ MPa at the inlet of WHUC. For details see [2]).

The geometry of the typical element is shown in Fig.3 and the dimensions of the channel are given in Table 1. Two designs are considered: a separator without hooks and a separator with hooks. The mean velocity at the inlet of the typical element of the wave-plate eliminator equals 1.5 m/s.

![Fig. 3. Scheme of the typical element of a wave-plate eliminator of the WHUC.](image)

**Table 1.** The dimensions of the channel.

| $H$, mm | $\alpha$, ° | $\lambda$, mm | $H_b$, mm | $W_b$, mm |
|---------|-------------|--------------|--------|--------|
| 9       | 117         | 19           | 0/4    | 0/4    |

The first series of calculations has been devoted to assessing the impact of droplet-size-distribution parameters on the separation efficiency of the separator without hooks. A Rosin–Rammler model [8] for the particle-size-distribution analysis was used. Three cases were tested: the constants in the Rosin-Rammler models were equal to 2.25 and 4.52 and the case of monodisperse particles. Fig. 4 shows the calculation results. It can be noted that narrowing of the droplet-diameter-distribution function results in an increasing separation efficiency.

![Fig. 4. Effect of particle-size distribution on the separation efficiency of the separation without hooks.](image)
Fig. 4 shows the influence of the particle-size-distribution parameters on the separation efficiency of the separator without hooks. A Rosin–Rammler model for the particle-size-distribution analysis was used. Three cases were tested: the constants in the Rosi-Rammler models were equal to 2.25 and 4.52 and the case of monodisperse particles. Fig. 4 shows the calculation results. It can be noted that narrowing of the droplet-diameter-distribution function results in an increasing separation efficiency.

Fig. 5 shows the influence of the mean velocity on the separation efficiency at a fixed value of a mean particle diameter of $d_{32} = 40 \, \mu m$. Its value was estimated using nozzle parameters and equations from [9]. The constant in the Rosi-Rammler model was equal to 4.52.

The next series of calculations was performed for various parameters at the inlet of the WHUC nozzle. Table 2 shows the results of the calculation.

**Table 2. Influence of inlet parameters of the WHUC.**

| $p_{in}$, MPa | $t_{in}$, °C | $G_0$, g/s | $\chi$ | $d_{32}$, μm | $E$ |
|--------------|-------------|------------|--------|--------------|-----|
| 10           | 257         | 317        | 0.139  | 40           | 0.81|
| 10           | 220         | 372        | 0.034  | 58           | 0.72|
| 10           | 300         | 214        | 0.259  | 37           | 0.81|
| 15           | 257         | 442        | 0.059  | 47           | 0.77|

For the basic WHUC parameters ($p_{in} = 10$ MPa, $t_{in} = 257$ °C), the effectiveness of particle separation for a separator with hooks increases to 99.6% from 81.3%.

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