The $R$ ratio in $e^+e^-$, the determination of $\alpha(M_Z^2)$ and a possible non-perturbative gluonic contribution

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Abstract. We review the determination of the QED coupling at the $Z$ pole, which is a crucial parameter for electroweak theory. We include recent $e^+e^-\rightarrow$ hadron data from Novosibirsk and Beijing to re-evaluate $\alpha(M_Z^2)$. We find $\alpha(M_Z^2)^{-1} = 128.973 \pm 0.035$ or $128.934 \pm 0.040$ according, respectively, to whether inclusive or exclusive $e^+e^-\rightarrow$ hadron data are used respectively in the interval $1.4 \leq \sqrt{s} \leq 2.1$ GeV. The error is mainly due to uncertainties in the data in the low energy region, $\sqrt{s} \leq 2.5$ GeV. We find that no advantage is obtained by analytic continuation of the dispersion relation into the complex $s$ plane. We show that the hints of structure for $\sqrt{s} \sim 2.5$ GeV may be evidence of a non-perturbative gluonic contribution to $R(s)$.

The value of the QED coupling at the $Z$ pole, $\alpha(M_Z^2)$, is the poorest known of the three parameters ($G_F, M_Z, \alpha(M_Z^2)$) which define the standard electroweak model. Indeed it is the precision to which we know $\alpha(M_Z^2)$ which limits the accuracy of the indirect prediction of the mass $M_H$ of the (Standard Model) Higgs boson [1].

The value of $\alpha(M_Z)$ is obtained from

$$\alpha^{-1} \equiv \alpha(0)^{-1} = 137.0359895(61)$$

using the relation

$$\alpha(s)^{-1} = \left(1 - \Delta\alpha_{\text{lep}}(s) - \Delta\alpha_{\text{had}}^{(5)}(s) - \Delta\alpha_{\text{top}}(s)\right) \alpha^{-1},$$

where the leptonic contribution to the running of the $\alpha$ is known to 3 loops

$$\Delta\alpha_{\text{lep}}(M_Z^2) = 314.98 \times 10^{-4}.$$  

From now on we omit the superscript (5) on $\Delta\alpha_{\text{had}}$ and assume that it corresponds to five flavours. We will include the contribution of the sixth flavour, $\Delta\alpha_{\text{top}}(M_Z^2) = -0.76 \times 10^{-4}$, at the end. To determine the hadronic contribution we need to evaluate

$$\Delta\alpha_{\text{had}}(s) = -\frac{\alpha_s}{3\pi} \int_{4m_t^2}^{\infty} P \frac{R(s')ds'}{s'(s'-s)}$$

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at $s = M_Z^2$, where $R = \sigma(e^+e^- \to \text{hadrons})/\sigma(e^+e^- \to \mu^+\mu^-)$.

The early determinations $^3$ of $\Delta\alpha_{\text{had}}(M_Z^2)$ made maximum use of the $e^+e^-$ measurements of $R(s)$, using the sum of the exclusive hadronic channels ($e^+e^- \to 2\pi, 3\pi, \ldots K\bar{K}, \ldots$) for $\sqrt{s} \sim 1.5$ GeV and the inclusive measurement of $\sigma(e^+e^- \to \text{hadrons})$ at larger energies. However, in the last few years the determinations of $\Delta\alpha_{\text{had}}$ from $^4$ have relied more and more on theoretical input. First perturbative QCD was used to better describe $R(\alpha)$ (where $R(\alpha) \equiv \alpha_\Delta$) for $\sqrt{s} > 3$ GeV in energy regions above the resonances to the next flavour threshold $^5$. Then, encouraged by the success of perturbative QCD to describe $\tau$ decay, it was used down to $1.8$ GeV, across a region with sparse data on $R(s)$, giving $^6$

$$\Delta\alpha_{\text{had}}(M_Z^2) = (277.5 \pm 1.7) \times 10^{-4},$$

where $\pm 10^{-4}$ comes from the uncertainty in perturbative QCD.

Recent methods to calculate $\alpha(M_Z^2)$ have used the analytic behaviour of $\Pi(s)$ in the complex $s$ plane. $\Pi$ is the hadronic contribution to the photon vacuum polarisation amplitude (or two-point correlator), where

$$\Delta\alpha_{\text{had}}(s) = -4\pi\alpha \text{Re}\Pi(s), \quad R(s) = 12\pi\text{Im}\Pi(s).$$

Groote et al. $^3$ introduce special polynomial weight functions, which are arranged to suppress data contributions in specific regions and to essentially replace them by perturbative QCD (together with non-perturbative gluon and light quark condensate contributions). For example, for a specific interval $(s_a, s_b)$, the idea is to deform the contour of integration so that the QCD contribution is evaluated around circular contours of radii $s_a$ and $s_b$, away from singularities on the $s_a, s_b$ cut. The accuracy of this approach was improved in $^8$ to give an error on $\Delta\alpha_{\text{had}}(M_Z^2)$ of $\pm 1.6 \times 10^{-4}$, close to the error of the straightforward estimate of $^3$.

We will see below that QCD does not reproduce the structure of the data for $R(s)$ in the $1.8 < \sqrt{s} < 3$ GeV region. This region itself gives at least an error of $\pm 10^{-4}$, which is additional to the errors of $^3, ^8$. If the QCD description fails to reproduce the data, in an average sense in this interval, then nothing is gained by deforming the contour of integration $^8$ using the trick of $^3, ^8$. It is just not possible to circumvent these measurements of $R(s)$, and their uncertainties, in this way.

In an interesting development Jegerlehner et al. $^9, ^10$ calculate the value of $\Delta\alpha_{\text{had}}$ at the large negative scale $s = -M_Z^2$ and then analytically continue around the large circle to positive $s = M_Z^2$. The QCD error comes mainly from the uncertainty in $\alpha_S(M_Z^2)$, and the neglect of $\alpha_S^4$ and higher order corrections. The extra error due to the analytic continuation around the large circle of radius $\sim M_Z$ is very small. At first sight it appears that we have dispensed with the data for $R(s)$ altogether, and hence determine $\Delta\alpha_{\text{had}}(M_Z^2)$ with an error $\lesssim 10^{-4}$ arising just from QCD.

Unfortunately there are sizeable errors in $\Pi(-s)$ due to the uncertainty in what to take for the light quark masses; even the uncertainty in the charm threshold, $4m_c^2$, gives a sizeable error. Moreover the constant term in the $\alpha_S^4$ contribution is not known yet. However these problems disappear for the derivative, the Adler function,

$$D(-s) = -12\pi^2 s \frac{d\Pi(-s)}{ds}$$

$^\dagger$ The QCD contribution was also evaluated around a circular contour in the $s$ plane in Ref. $^5$.

$^\ddagger$ Due to Cauchy’s theorem the result is independent of the choice of contour.
or for the discontinuity
\[ R(s) = \frac{6\pi}{i} \text{disc}\Pi(s) = 12\text{Im}\Pi(s). \] (8)

Indeed this was recognized in [1] where \( D \) was evaluated for negative \( s \) using perturbative QCD (and parton condensate contributions). These authors checked that the theoretical values for \( D(-s) \) in the space-like region agree well with the "direct" evaluation in which the data for \( R(s) \) are used to determine \( \Delta\alpha_{\text{had}}(-s) \). The agreement was found to be good even for \( \sqrt{s} \) as low as 2 GeV. Unfortunately this is for the derivative, and not the value, of \( \Delta\alpha_{\text{had}} \). To determine \( \alpha(M_Z^2) \) Jergerlehner therefore evaluates

\[ \Delta\alpha_{\text{had}}(-M_Z^2) = \left[ \Delta\alpha_{\text{had}}(-M_Z^2) - \Delta\alpha_{\text{had}}(-s_0) \right]^{\text{QCD}} + \Delta\alpha_{\text{had}}(-s_0)^{\text{data}} \] (9)

where the QCD contribution is accurately known in terms of \( D \) and so the error in \( \alpha(M_Z^2) \) dominantly reflects, once again, the error in the data for \( R(s) \). The evaluation can be done for any \( \sqrt{s_0} \gtrsim 2 \) GeV. Jergerlehner chooses \( \sqrt{s_0} = 2.5 \) GeV and finds

\[ \Delta\alpha_{\text{had}}(M_Z^2) = \Delta\alpha_{\text{had}}(-M_Z^2) + (0.45 \pm 0.02) \times 10^{-4} \]
\[ = (277.82 \pm 2.54) \times 10^{-4}, \] (10)

where the error is entirely attributed to that on \( \Delta\alpha_{\text{had}}(-s_0) \).

Since the error in \( \alpha(M_Z^2) \) is driven by the data for \( R(s) \), it is relevant to discuss the new and forthcoming measurements. First, the CND-2 and SND experiments at VEPP-2M at Novosibirsk have made precision measurements of a wide range of exclusive processes in the interval \( 0 < \sqrt{s} < 1.4 \) GeV [10, 11]. For example, the measurement of \( e^+e^- \rightarrow \pi^+\pi^- \) [11] has considerably improved precision such that, together with chiral perturbation theory, we find that the error in the \( 2\pi \) contribution to \( \Delta\alpha_{\text{had}} \) for \( \sqrt{s} < 0.96 \) GeV is reduced to about \( \pm 0.5 \times 10^{-4} \), see Table 1.

The second source of new information is the Beijing \( e^+e^- \) collider, where BES II are making direct measurements of \( R(s) \) for \( 2 < \sqrt{s} < 5 \) GeV. So far values of \( R(s) \) at six values of \( \sqrt{s} \) have been published [13]. The two lowest values (\( \sqrt{s} = 2.6, 3.2 \) GeV) are shown in Fig. 1, together with preliminary BES II data [14]. These data, taken together with the compatible earlier \( \gamma\gamma \) data [15], indicate the existence of a "dip-bump" type structure in the measurements of \( R(s) \) about the \( O(\alpha^2) \) perturbative QCD prediction shown by the continuous curve, see Fig. 1. The bump appears to be at \( \sqrt{s} \sim 2.6 \) GeV and the dip at \( \sqrt{s} \sim 2 \) GeV. This apparent structure leads to an uncertainty in \( \Delta\alpha_{\text{had}} \). Interestingly, the contributions to the right-hand-side of (9) from the interval \( 1.8 < \sqrt{s} < 3 \) GeV obtained using for \( R(s) \) (i) the interpolation through the data and (ii) the perturbative QCD prediction are

\[ \Delta\alpha_{\text{had}}^{1.8-3 \text{ GeV}}(M_Z^2) = 17.77 \pm 1.80 \quad \text{and} \quad 17.35 \pm 0.13, \] (11)

respectively, in units of \( 10^{-4} \). That is the results are very similar, which looks reasonable from the hadron-parton duality and QCD sum rule viewpoint. We take the data value and so, in fact, the uncertainty from this domain may be less than our pessimistic estimate.

In the energy intervals described by perturbative QCD (\( 3 < \sqrt{s} < 3.74 \) GeV and \( \sqrt{s} > 5 \) GeV) we use both the two-loop expression with the quark mass explicitly included and the massless three-loop expression [16] calculated in the \( \overline{\text{MS}} \) scheme.
Figure 1. A plot of the ratio $R(s)$ versus $\sqrt{s}$ in the most sensitive $\sqrt{s}$ interval. Up to $\sqrt{s} = 2.125$ GeV we show by continuous lines the upper and lower bounds of the sum of exclusive channels. Above $\sqrt{s} = 1.4$ GeV we show the exclusive measurements of $R(s)$, together with the interpolation (dashed curve) used in (4). We show six preliminary BES-II points, which were not used in the analysis, together with two published points which were used. The central perturbative QCD prediction is also shown. In the region $1.46 < \sqrt{s} < 2.125$ GeV we used, in turn, the inclusive and exclusive data to evaluate $\Delta \alpha_{\text{had}}$.

In addition to the above we include the perturbative QCD error coming from varying $m_c, m_b, M_Z$ within the uncertainties quoted in the [18], $\alpha_S(M_Z^2) = 0.119 \pm 0.002$ and varying the scale $\alpha_S(cs)$ in the range $0.25 < c < 4$.

† The uncertainty due to using a different scheme may be estimated to be of the order of the $O(\alpha_S^4)$ correction, which is about $3 \sum e_i^2 r_3^2 (\alpha_S/\pi)^4$. We may take $r_3 = -128$ [17] which leads to an uncertainty much smaller than that given in Table 1.

‡ We thank Thomas Teubner for valuable discussions concerning the perturbative QCD contribution.
By far the largest uncertainty comes from the region 1.4 < \sqrt{s} < 3 \text{ GeV}. The recent Novosibirsk measurements have considerably improved the exclusive data below 1.4 \text{ GeV}, but above 1.4 \text{ GeV} we see from Fig. 1 that the sum of the exclusive channels exceeds the inclusive measurements of \text{R}. We therefore evaluated the contribution in the region 1.46 < \sqrt{s} < 2.125 \text{ GeV} using first the inclusive data for \text{R} and then using the sum of the exclusive channels. (We checked that our results for the contributions from the exclusive channels were in agreement with the detailed table of results given in Ref. [13], if we were to omit the new Novosibirsk data and to include the \tau data.)

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|}
\hline
$s'$ interval (GeV) & $s = M_Z^2$ & $s = -6 \text{ GeV}^2$ & $s = -M_Z^2$ \\
\hline
$2m_\pi - 1.46^a$ & $38.18 \pm 0.52$ & $34.24 \pm 0.48$ & $38.18 \pm 0.52$ \\
1.46 - 2.125 & $11.80 \pm 0.94c$ & $7.80 \pm 0.60c$ & $11.79 \pm 0.94c$ \\
 & $(14.59 \pm 1.76^b)$ & $(9.59 \pm 1.14^b)$ & $(14.58 \pm 1.76^b)$ \\
2.125 - 3 & $13.05 \pm 1.22^c$ & $6.33 \pm 0.58^c$ & $13.03 \pm 1.22^c$ \\
3 - 3.74^d & $7.41 \pm 0.04$ & $2.58 \pm 0.01$ & $7.39 \pm 0.04$ \\
3.74 - 5 & $15.11 \pm 0.50$ & $3.64 \pm 0.12$ & $15.04 \pm 0.50$ \\
5 - $\infty^d$ & $170.06 \pm 0.66$ & $6.09 \pm 0.03$ & $169.83 \pm 0.44$ \\
$\omega, \phi, \psi', \Upsilon'$ & $18.57 \pm 0.57$ & $11.26 \pm 0.27$ & $18.52 \pm 0.57$ \\
$\Delta\alpha_{\text{had}}^{(b)} \times 10^4$ & $274.18 \pm 2.52$ & $71.94 \pm 1.40$ & $273.78 \pm 2.47$ \\
 & $(276.97 \pm 2.90)$ & $(73.73 \pm 1.82)$ & $(276.57 \pm 2.85)$ \\
\hline
\end{tabular}
\caption{Contributions to $\Delta\alpha_{\text{had}}(s) \times 10^4$ of \cite{4} coming from the different $\sqrt{s'}$ intervals for three different values of $s$. The alternative values in the round brackets take the summation of exclusive channels as the contribution from the region 1.46 - 2.125 GeV, rather than that from the inclusive data for $R(s')$.}
\end{table}

\begin{itemize}
\item The upper (lower) error corresponds to the 2\pi (remaining) exclusive channels.
\item Errors with identical superscripts are added linearly. The remaining errors are added in quadrature.
\end{itemize}

The results for $\Delta\alpha_{\text{had}}(s)$ of \cite{4} are shown in Table 1 not only for $s = M_Z^2$, but also for two space-like values $s = -s_0 = -6 \text{ GeV}^2$ and $s = -M_Z^2$ in order to study Jegerlehner’s approach \cite{11}. We see that indeed the error on the space-like evaluation at $s = -6 \text{ GeV}^2$ is reduced in comparison to that for $s = \pm M_Z^2$; as expected from the form of \cite{4} the error mainly arises from uncertainties in the data for $R(s')$ with $s' \lesssim |s_0|$. However before we can take advantage of this reduction we must consider the error in the perturbative continuation from $s = -s_0$ to $-M_Z^2$. (It is reasonable to assume that the error in going round the circle to $s = M_Z^2$ is much smaller.) To estimate the error in the difference $\Delta\alpha_{\text{had}}(-M_Z^2) - \Delta\alpha_{\text{had}}(-s_0)$ we use the pure perturbative expression for $R(s')$ in the whole interval of $s'$. The resulting uncertainty is the order of $\pm 1 \times 10^{-4}$ and so in practice there is only a marginal gain from the space-like evaluation. Until this theoretical error is more accurately quantified, we take a conservative approach and use the error of the $s = M_Z^2$ determination of $\Delta\alpha_{\text{had}}(M_Z^2)$.

Let us return to the dip-bump structure in $R(s)$ in the region $2 < \sqrt{s} < 3 \text{ GeV}$, see Fig. 1. This was not expected, at least from the quark states; recall the success at

\footnotetext[1]{The inclusive measurements of the $\gamma\gamma2$ collaboration (with radiative corrections included) at higher energies appear consistent with the new Beijing measurements, which would tend to favour the inclusive input leading to a smaller value of $\Delta\alpha_{\text{had}}$.}

of the perturbative QCD description of $\tau$ hadronic decay. Charm is too heavy, and the light quarks too light to produce such a broad structure. Perturbative QCD was expected to reproduce the $R(s)$ data in this $\sqrt{s}$ interval. However at $\mathcal{O}(\alpha_s^2)$ we open up the 3-gluon contribution, see Fig. 2, and we may expect some structure due to this channel. Indeed lattice computations predict a $J^P = 1^-$ glueball with mass typically in the range 3.3–4 GeV \[20\]. So non-perturbative gluonic structure at $\mathcal{O}(\alpha_s^3)$, and higher order, may be anticipated in the region up to 4 GeV. In this connection we note that the non-perturbative (condensate) contribution to the Adler function $D(-s)$ diverges for values of $\sqrt{s} \lesssim 2$ GeV, even in the space-like region \[9\]. Recall in the

\[Figure 2. \quad \mathcal{O}(\alpha_s^3)\) three gluon contribution to $R$. The contribution of the light quarks cancel as $\sum e_q = 0$ for $q = u, d, s$, so we are left with the $c$ quark contribution.

phenomenological description of the decay $J/\psi \to gg\gamma$ that it was crucial to introduce an effective gluon mass of about 800 MeV to reproduce the $\gamma$ energy spectrum \[21\]. A similar result holds for $\Upsilon$ and $Z$ decays \[22, 23\]. We thus anticipate an effective threshold for the 3 gluon contribution to $R(s)$ at $\sqrt{s} \simeq 2.4$ GeV. This effective gluon mass is also consistent with the predicted 1.6 GeV mass of the lightest (0$^{++}$) glueball. More or less the same position of the threshold in $R(s)$ is obtained assuming that the hadronization of the 3 gluon contribution to $R$ (cut A in Fig. 2) proceeds through the 6-quark channel. In the threshold region we must use the constituent quark mass, so that the 3 gluon channel opens at $\sqrt{s} \gtrsim 6M_{\text{constit}} \simeq 2.1$ GeV.

Fig. 2 has not only the possibility of a gluon cut, but instead may be cut across the $q\bar{q}$ state, cut B. With respect to this latter cut, the imaginary part in the gluon channel plays the role of an absorptive correction. Therefore the diagram may give a negative $q\bar{q}$ contribution and a positive 3g contribution leading to a non-trivial structure\[1\]. In addition there may be mixing, and mass shifts, of the $J^P = 1^{--}$ glueball and $q\bar{q}$ resonant states. Of course the amplitude of this gluonic-driven structure cannot be too large as it originates from $\alpha_s^3$ and higher order graphs. However the non-perturbative 3 gluon interactions are strong enough to produce a resonant type structure in the relevant $\sqrt{s}$ region with up to about 10% oscillations, and seen in Fig. 1. Note that the non-perturbative contribution to the Adler $D$ function becomes large at $\sqrt{|s|} \sim 2$ GeV even in the space-like region \[3\]. If the bump is due to 3-gluon production then we expect a larger yield of $\eta'$ or $\eta$ mesons (which are strongly coupled to gluons) in this energy region \[24\].

We conclude that it is important to use the experimental measurements of $R(s)$ to calculate $\Delta\alpha_{\text{had}}$ and its error. One can replace the data for $R(s)$ in a specific region by

\[† \quad \text{Recall the cusp structure for a resonance occurring near a threshold in multichannel processes.} \]

\[‡ \quad \text{Estimated from the difference between } \mathcal{O}(\alpha_s^3) \text{ and } \mathcal{O}(\alpha_s^2) \text{ QCD expectations.} \]
the QCD prediction only after we understand the origin of all structure in the region, and are confident that our QCD approximation is sufficient to account for the effects. For example, much accuracy is gained by replacing the data measurements for $R(s)$ above the $\Upsilon$ resonance region by the $O(\alpha^3_S)$ QCD prediction. However we have seen that a similar replacement around the charm threshold is not so clear. The theoretical uncertainty due to the charm mass and the (more than two-loop) non-perturbative interaction may be larger than the accuracy of the data. From the presently available data we find (see Table 1)

$$\Delta\alpha^{(5)}_{\text{had}}(M^2_Z) = 274.18 \pm 2.52 \text{ or } 276.97 \pm 2.90$$

(according to whether the inclusive or exclusive data are used in the interval $1.46 < \sqrt{s} < 2.125$ GeV. When used in (2) these values correspond to a value of the QED coupling at the $Z$ pole of

$$\alpha(M^2_Z)^{-1} = 128.973 \pm 0.035 \text{ or } 128.934 \pm 0.040$$

respectively. It may be argued that the first value is favoured, since the $\gamma\gamma 2$ inclusive data appear to agree with the new Beijing measurements at higher energies, see Fig. 1.

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