Estimating Service Lives of Organic Vapor Cartridges III: Multiple Vapors at All Humidities

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A published model for estimating service lives of organic vapor (OV) air-purifying respirator cartridges has been extended to include multiple organic vapors at all humidities. Equilibria among the OVs are calculated using Ideal Adsorbed Solution Theory, whereas the effects of adsorbed water are considered as due to micropore volume exclusion. Solubilities of OVs in water must also be taken into account. Adsorption kinetics of components of mixtures are based on published correlations of the effects of covapors and water vapor. The dynamics of adsorption and competition are incorporated using expanding zones within the carbon bed, taking into account vapor and water displacements. Measurements of breakthrough curves for two ternary OV mixtures at high humidities have been done for a single cartridge type. The service life estimation model, implemented as a spreadsheet and a computer program, has been tested against these data as well as data for OV mixtures from literature sources. Good agreements were obtained between model predictions and experimental breakthrough times at dry conditions and humid conditions.

Keywords cartridge, mixtures, organic vapor, respirator, service life

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INTRODUCTION

In the absence of end-of-service life indicators for organic vapor (OV) air-purifying respirator cartridges, measurements, and/or predictive models must be relied on to set required change-out schedules.¹ Previous reports have presented models for estimating service lives of OV cartridges for single organic vapors² and of other cartridges for reactive gases,³ both at all humidities. Since there are mixtures of OVs present in some workplaces, there is still a need to take into account the competitive interactions of multiple vapors with each other and with water.

Several researchers have measured breakthrough times or breakthrough curves for mixtures (usually binary and dry) of OVs with respirator cartridges. However, most of these studies were performed with binary mixtures at dry conditions. Additional data for multivapor mixtures at high humidities are needed to develop and test service life predictive models.

The scope of the work presented here is to extend the previous equation-based, single-vapor model to handle mixtures of vapors at all humidities. Published data for OV mixtures and cartridges were identified for testing this model. New breakthrough time data for OV mixtures at high humidities were developed for comparisons with model predictions. The practical goal of the model presented here is to be able to predict when cartridges no longer provide a worker with adequate protection. Estimations of breakthrough times for each vapor component at selected acceptable breakthrough limits can be applied to estimate service lives and (perhaps with a safety factor) set change-out schedules.

BACKGROUND

In 1998 the Occupational Safety and Health Administration published two rules of thumb based on the best information available at the time:

Where the individual compounds in the mixture have similar breakthrough times (i.e., within one order of magnitude), service life of the cartridge should be established assuming the mixture stream behaves as a pure system of the most rapidly migrating component or compound with the shortest breakthrough time.²²

Predictions based upon models without experimental data should probably be very conservative and ascribe the service life derived from the least well adsorbed compound to the total mixture concentration in terms of parts per million. The displacement of a less well adsorbed compound by a more highly adsorbed one may alter the actual service life from the estimated one in some cases.²³
These guidelines reflect the expected phenomena of competition and displacement but are confusing to understand and apply and may be overly conservative.

Equation-based models for estimating service lives of OV cartridges have been published for single vapors at dry and all-humidity conditions. They are based on the Reaction Kinetic form of the Wheeler-Jonas equation:

$$t_b = \frac{W_c W}{C_o Q \ln \left( \frac{C_o - C}{C} \right)}$$  \tag{1}

which includes (1) carbon bed parameters of bed weight $W$ (g) and packed density $\rho_B$ (g/cm³); (2) use parameters of challenge vapor concentration $C_o$ (g/cm³), breakthrough concentration $C$ (g/cm³), and airflow rate $Q$ (cm³/min); and (3) vapor/carbon interaction parameters of adsorption rate coefficient $k_v$ (min⁻¹) and adsorption capacity $W_e$ (g/g carbon) at $C_o$. With these units, breakthrough time $t_b$ is in minutes. A computer application has been distributed for the single-vapor, all-humidity model.

These models also rely on the Dubinin-Radushkevich (DR) equation to calculate equilibrium adsorption capacity $W_e$ (g/g carbon) of individual organic vapors:

$$W_e = \frac{W_o d_L \exp \left[ - \left( \frac{RT}{\beta E_o} \right)^2 \left( \ln(p_{sat}/p) \right)^2 \right]}{\rho_B}$$  \tag{2}

where $W_o$ (cm³/g) is the micropore volume of the carbon and $E_o$ (K/mol) is its reference adsorption energy; $d_l$ (g/cm³) is the liquid density of the adsorbate; $p_{sat}$ is the vapor pressure of its unadsorbed bulk (liquid) form at temperature $T$ (°K); and $\beta$ is its relative affinity coefficient (no units).

At high humidities, such capacities are reduced by micropore volume exclusion by adsorbed water, whereas an opposite effect is to increase capacities by solubility (if any) in this water. The single-vapor model used published correlations of adsorption rates of both OVs and water, an expanding zone concept with water vapor rollup due to displacement by OVs, and other effects of water and OVs on adsorption rates and capacities.

Two reviews of equilibrium adsorption of binary mixtures identified the best equations for estimating capacities. Twelve adsorption isotherm equations proposed for describing multicomponent adsorption were tested with two sets of binary mixture data. Of these, the Grant-Manes (Polanyi Adsorption Theory) and the Myers-Prausnitz (Ideal Adsorbed Solution Theory, IAST) were the most successful, especially when combined with the DR equation. Studies with additional mixture data confirmed the usefulness of the IAST/DR approach supplemented with Bering or Lewis equations.

A study of the effects of OV covapors on adsorption rates produced average correction factors based on the order of elution from carbon beds. Adsorption rate coefficients for first eluting vapors in mixtures were statistically no different than those of single vapors. Correction factors (rate coefficient multipliers for components of a mixture) for second eluting vapors averaged 0.85 and those for third and fourth eluting vapors averaged 0.56.
to their experimental multicomponent breakthrough curves of each vapor \( i \) in a mixture to extract empirical constants \( k'_i \) and breakthrough curve midpoints \( \tau_i \) for challenge concentrations \( C_{oi} \) and breakthrough concentrations \( C_i \). The mixtures included acetone/m-xylene, acetone/cyclohexane/toluene, ethyl acetate/cyclohexane/toluene, cyclohexane/toluene/m-xylene, ethyl acetate/cyclohexane/toluene/m-xylene, and acetone/cyclohexane/toluene/m-xylene.

Displacement ratios and displacement fractions were also calculated from observed concentration rollups. With only a few parameters, this model was able to describe the breakthrough curves; however, these parameters were calculated from the same breakthrough curves. Therefore, this was a descriptive model instead of a predictive one.

A predictive multicomponent model would need to develop values for these parameters from independent sources, e.g., single and multiple component adsorption isotherms and rate coefficient models. Vahdat et al.\(^{20}\) have taken just such an approach to transform the Yoon/Lara model\(^{16−19}\) into a predictive model. They used Langmuir isotherms extracted from single-component breakthrough curves to obtain parameters to apply the IAST mixture model. Rate coefficients were obtained from single-component breakthrough times at 0.001 and 0.999 breakthrough fractions, which assumes symmetric breakthrough curves and the Wheeler/Reaction Kinetic (Eq. 1) model. This approach still lacks the ability to predict the single vapor adsorption capacity and rate parameters needed in a predictive model.

**New Model Description**

**Expanding Zone Model**

The model presented here is based on a concept of zones within the carbon bed first introduced in the single-vapor, all-humidity model.\(^{12}\) These expanding zones are defined differently from those of Cooney and Strusi,\(^{15}\) having zone boundaries at the centers of the mixture component wavefronts and breakthrough curves. This allows handling vapor capacities and adsorption kinetics separately. Figures 3 and 4 show the new zone definitions.

Figures 5 and 6 show a hypothetical example of the expanding zone model for five vapors. Initially, the kinetics are ignored and the component wavefronts are taken to be flat. At the beginning of cartridge or carbon bed exposure, all zones but Zone 6 have zero width (depth into the carbon bed). With time of exposure to vapors, they expand at differing rates to different widths (not the same widths as shown in the figures). The boundaries are where one of the vapors in succession is completely adsorbed and does not pass into the next zone.

For this example, five vapors at 500 ppm each are flowing into Zone 1 and maintained at these concentrations in the gas phase (Figure 5). (Note that the order in the legend is the stack order in the figures.) In the carbon phase (Figure 6), however, much more of the heptane with the highest adsorption affinity is adsorbed and much less of the methanol is retained. At some distance into the bed all the heptane is removed and only the other four vapors pass into Zone 2. This process continues until no OVs are left to pass into Zone 6. Zone 1 width increases with time as more vapors enter. Other zones expand similarly until they each in turn reach the end of the bed and an equilibrium breakthrough of each vapor occurs.

This reduces the problem to determining the equilibrium adsorbed capacities and gas phase concentrations of the vapor components in each zone. The IAST/DR/Bering equations (detailed below) provide the former.\(^{11}\) Gas phase vapor concentrations in Zone 2 are increased by displacement of some of the vapors already adsorbed in Zone 2 by the OVs adsorbing in the expanding Zone 1 (in this example, mostly heptane). These vapor concentration increases (rollups) raise the capacities in Zone 2 and subsequent zones. Applying the principle of mass balance (total amounts of each vapor adsorbed in all the zones equals total amounts entering the
The Bering equation and Raoult’s Law (Ideal Adsorbed Solution) provide total molar capacity, \( n_T \), for each zone mixture by mole fraction weighting of affinity coefficient \( \beta_T = \sum x_i \beta_i \), partial liquid molar volume \( \bar{V}_{mi} \), and adsorption potential \( \epsilon_T = \sum X_i \epsilon_i = \sum x_i \beta_i R T \ln[x_i p_{sati}/p_i] \) parameters of the components:  
\[
\frac{W_o}{V_{mT}} \exp\left[-\frac{(RT/\beta_Eo)^2}{2} \left( \sum x_i \ln(x_i p_{sati}/p_i) \right)^2 \right] \quad (6)
\]
Component molar capacities are \( n_i = x_i n_T \). Volume of adsorbed mixture is \( V_{adsOV} = V_{mT} n_T \).

**OV Rollups**

Zone 1 is exposed to the entering OV concentrations; subsequent zones (\( z > 1 \)) may be exposed to higher concentrations due to displacements of previously adsorbed vapors by more strongly adsorbed OVs. By mass balance the extent of concentration (g/cm³) rollup depends on the airflow \( Q \), the average speed of a zone movement \( W/\tau_z \) (g/min), and the differences in volumetric adsorption capacities (cm³/g) of OVs in adjacent Zones \( z \) and \( z + 1 \):  
\[
\text{RollupC}_{oi(z+1)} = \text{RollupC}_{oi(z)} + \left( \frac{V_{adsOVi(z+1)} - V_{adsOVi(z)}}{W_{dLi}} \right) Q \tau_z \quad (7)
\]
where \( \tau_z \) is the equilibrium breakthrough time of Zone \( z \) for carbon bed weight \( W \) and \( d_{Li} \) is liquid density of component \( i \). Because of rollup effects, all the \( C_{oi} \) are replaced by \( \text{RollupC}_{oi} \) in each Zone \( z > 1 \) to calculate \( V_{adsOV} \) by the above equations. This is best accomplished by iterative computations.

**Water Vapor Capacity**

Water vapor is less efficiently adsorbed on carbon than OVs and much of it passes completely through the bed. All zones are exposed to any humidity that may be in the air and water may adsorb in each of them, reducing the micropore volumes available to the OVs. In the absence of OVs, the volume (cm³/g carbon) of water adsorbed at equilibrium with relative humidity \( RH = p_{H2O}/p_{satH2O} \) air can be described by the DR equation:  
\[
V_{adsH2O} = W_o \exp\left\{-\left( \frac{RT}{\beta_{H2O} E_o} \right)^2 \right( \ln(RH) \right)^2 \} \quad (8)
\]
with the unitless water affinity coefficient \( \beta_{H2O} \), a property of the carbon, in the range of 0.06. (2)

Because water adsorbs slowly on activated carbon, its equilibrium will be approached only with increasing time of exposure to humid air. The extent (fraction) of equilibrium reached at time \( t \) is:  
\[
\text{Fract}_{H2O} = \left( 1 - \exp\left\{-0.00005(T - 273.15) v_L T \right\} \right) \quad (9)
\]
where linear air flow velocity \( v_L \) is in cm/s, bed depth \( d_B \) is in cm, time \( t \) is in min, and \( \Delta A_{tot} \) (g/g carbon) is the difference (+ or −) between two equilibrium water capacities.
The capacities at the exposure RH (Run RH) and at the RH (Pre RH) at which the carbon was previously equilibrated are obtained from applying the DR equation. For equilibrium or the same RH, this fraction is 1.00. Otherwise, it is applied to the difference in equilibrium water volumetric capacities, so that:

\[ V_{\text{adsH}_2\text{O}} = V_{\text{ads}}(\text{Pre RH}) + \text{Fract}_{\text{H}_2\text{O}}[V_{\text{ads}}(\text{Run RH}) - V_{\text{ads}}(\text{Pre RH})] \]

**Water Vapor Rollup**

Zone 1 is exposed to the entering water vapor concentration; subsequent zones \((z > 1)\) may be exposed to higher humidities from water rollup effects due to displacements of previously adsorbed water by OV s. The extent of RH rollup is calculated from water rollup effects due to displacements of previously adsorbed from the aqueous phase, which is otherwise excluding the OV . The presence of condensed water enhances the capacity, improves retention, and extends breakthrough times of a water soluble OV, at least compared with what these would be if the OV were not water soluble. The OV adsorption potential in the presence of air at relative humidity RH is:

\[ \varepsilon_RH = \left( \frac{RTV_m}{\gamma h - 0.28} \right) \left[ \frac{1}{V_m} \ln \left( \frac{p_{\text{sat}}}{p} \right) - \frac{1}{18} \ln \left( \frac{1}{\text{RH}} \right) \right] \]

where \(\gamma_h = 4.24\) \((\text{P}_e/V_m)\) for OV molar volume \(V_m\) and molar polarizability \(P_e\) is the scale factor of an OV relative to heptane. For a completely water miscible OV in a water volume of \(V_{\text{adsH}_2\text{O}}\) (calculated from Eqs. 8–13) the volume of OV adsorbed from the aqueous phase is:

\[ V_{\text{adsOV}} = V_{\text{adsH}_2\text{O}} \exp[-(\varepsilon_RH/\beta_{\text{OV}E_o})^2] \]

For a less soluble OV this is multiplied by a solubility factor \(S_f\) defined as the fraction in parts by liquid volume of OV that can be dissolved in one part of water volume. The range of \(S_f\) is taken to be from zero for a totally immiscible OV to 1.0 for a totally miscible one. A conservative estimate for \(S_f\) is zero, but this should not be used for alcohols, amines, or other polar compounds, which are often to some extent water-soluble.

The total gravimetric capacity \((\text{g/g carbon})\) of the activated carbon for the OV in the presence of adsorbed water then becomes:

\[ W_c \text{OVtotal} = (V_{\text{adsOV}} + V'_{\text{adsOV}})d_L \]

**Effects of Water on OV Mixture Capacity**

Having the parameters and equations to calculate the independent volumetric capacities of an OV and pure water, it becomes necessary to calculate capacities when both are adsorbed on activated carbon. The Volume Exclusion Theory provides:

\[ V_{\text{adsOV}} = (W_o - V_{\text{adsH}_2\text{O}}) \exp \left\{ -\left( \frac{RT}{\beta_{\text{OV}E_o}} \right)^2 \left( \ln \frac{p_{\text{satOV}}}{p_{\text{OV}}} \right)^2 \right\} \]

\[ V_{\text{adsH}_2\text{O}} = (W_o - V_{\text{adsOV}}) \exp \left\{ -\left( \frac{RT}{\beta_{\text{H}_2\text{O}E_o}} \right)^2 \left( \ln \frac{p_{\text{satH}_2\text{O}}}{p_{\text{H}_2\text{O}}} \right)^2 \right\} \]

for equilibrium volumes \((\text{cm}^3/\text{g})\) of the two adsorbates competing for available micropore volume \(W_o\). Note that \(p_{\text{H}_2\text{O}}/p_{\text{satH}_2\text{O}}\) is relative humidity RH. These two linear equations can be solved analytically for the adsorbed volumes \(V_{\text{adsH}_2\text{O}}\) and \(V_{\text{adsOV}}\).

**Water Solubility**

One more contribution to \(V_{\text{adsOV}}\) needs to be included, that due to solubility, if any, of an OV in the adsorbed water phase, which is otherwise excluding the OV. The presence of

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Skew corrections are used to calculate rate coefficients at other breakthrough fractions (up to $C/C_0 = 0.5$) as:

$$ k_{v(C/C_0)} = \left[ 1 + b \ln(C_0/C - 1) \right] k_{v0.1\%} $$

(18)

where $b$ is a quadratic root solution of a correlation for the skew parameter $S = k_{v1\%}/k_{v10\%}$:

$$ S = 1.41 - 0.0000324 \left[ \frac{1 + b \ln(9)}{1 + b \ln(C_0/C - 1)} \right] k_{v(C/C_0)} $$

(19)

which has a lower limit $S \geq 1$.

Next, rate coefficient correction factors reported by Wood for orders of elution are applied to the resulting $k_{v(C/C_0)}$: 1.00 for first eluting, 0.85 for second, and 0.56 for subsequent.

Because adsorbed water has an effect on OV adsorption rates the OV adsorption rate coefficient is further corrected by:

$$ k_{v(C/C_0)}^{Wet} = 0.3 + 0.7 \left( \frac{W_{Wet}}{W_{Dry}} \right) k_{v(C/C_0)}^{Dry} $$

(20)

This has an upper limit of $k_{v(C/C_0)}^{Dry}$.

**Model Application**

Because there are many interacting effects between the OVs and water vapor, application of this model, such as in a spreadsheet or computer program, requires iterations to attain a final answer. First, water presence and vapor rollups are ignored. During repeated iterations, OV rollup in each zone is calculated, increasing vapor concentrations and adsorbed concentrations. After iterations produce fixed OV capacities in each zone, water vapor is introduced and its effects calculated. Further iterations with water vapor included are repeated until fixed capacities and breakthrough times result. The input parameters required are the same as with the single vapor model and program: (1) cartridge and carbon parameters, (2) organic vapors and water parameters, and (3) use condition parameters. See input parameter descriptions with Eqs. 1 and 2 above.

**Experimental**

The 3M cartridge used in this work (#7251; 3M St. Paul, Minn.) has a cylindrical geometry for which it was easy to construct a gastight holder (described below) for testing. Cartridges were used as received, one at a time. Carbon bed dimensions were reported by the manufacturer to be 7.6 cm diameter and 2.25 cm deep for 44.5 g of adsorbent. These are also the parameters used in the model, along with a calculated packed density of 0.436 g/cm$^3$. The carbon granules were reported by the manufacturer to be 12–16 mesh, so an average diameter of 0.14 cm was used in the model. Chemicals used were ACS certified reagents or better.

The experimental apparatus is diagrammed in Figure 7. A Miller/Nelson Flow-Temperature-Humidity Control System (model HCS-401; Miller-Nelson Research, Inc., Monterey, Calif.) was used to generate a constant air source of known temperature and relative humidity. Compressed air filtered for organics and particulates fed the Miller/Nelson unit. Water used by the Miller/Nelson unit was tap water that was run...
through a deionizing cartridge prior to use. The output from the Miller/Nelson was vented into a large plastic carboy with a volume of approximately 20 liters. This was used as a reservoir from which conditioned air could be drawn. The input was maintained at a substantially greater rate (60 L/min) than output so that dilution with outside air did not occur.

The intake of a breathing simulator pump (model SH55E, Scott Aviation Corporation, Lancaster, N.Y.) was inserted into the carboy to extract 33 to 37 L/min of conditioned air at 25 cycles per min. The breathing pump was used with a cam to simulate the pulsed effect that occurs during the human breathing cycle. The exhalation cycle flow was vented to the atmosphere to simulate respirator operation with an exhalation valve and a backflow valve to prevent reverse flow through the cartridge. The effluent stream from the pump was ultimately connected to the cartridge holder.

Before that connection, a tee was placed in the air line so that liquids could be introduced to produce vapor in the airstream. The tee was wrapped with heating tape to slightly elevate the temperature so the liquid contaminants would flash evaporate on entering the gas stream. There was sufficient distance from the tee to the cartridge to allow cooling to ambient temperature. Liquid chromatographic (LC) pumps (model 210, SRI Instruments, Inc., Torrance, Calif.) were used to dispense the liquid chemicals. The effluent streams of the pumps were connected in parallel so that varying amounts of liquids could be independently controlled to yield various concentrations of vapors in the gas stream. For the results reported here, one or three pumps were used at a time. After the vapor was introduced, the airstream passed through a sealed 5-L container to provide mixing for uniform concentrations.

The vapor(s) in the airstream from the mixing container then passed into an aluminum housing that held the cartridge to be tested. This housing was a two-piece system clamped together with an o-ring around the cartridge to provide a leak-proof fit. The incoming gas stream to the cartridge holder was tapped with a 1/8-inch Teflon tube connected to a gas chromatograph. A similar connection was made to the stream exiting the holder. This provided a means to monitor the vapor concentrations entering and exiting the cartridge being tested.

The vapor monitor consisted of an SRI model 8610 dual-column, dual-flame detector, gas chromatograph (GC) also manufactured by SRI, Inc. It was equipped with two 10-port automated valves with 1 mL sample loops. It used PeakSimple software provided by SRI, Inc. The GC could be programmed to automatically sample the two (cartridge input and output) gas streams, quantify the concentrations, and store the values in an Excel spreadsheet for future use. The columns, RTX-5, 30 m long x 0.053 mm ID and 1.0-micron film thickness (Restek, Bellefonte, Pa.) were operated at 120°C and 5-mL/min hydrogen carrier flows. All components could be separated in under 3 min. This permitted simultaneous monitoring of the input and exhaust of the cartridge at 3-min intervals.

The GC responses for each chemical vapor were calibrated by using standards produced in the laboratory as follows. A 10-L gas bag was filled with 6 L of air. An appropriate amount of solvent was injected using a microliter liquid syringe. The vapor and air were mixed by kneading the gas bag. A sample of the standard was injected into the gas sampling loop of the gas sampling valve. Thus, the same plumbing was used for calibration and analysis of unknowns. This was done at a frequency of once or twice a day depending on the length of analysis time. In all cases, the GC was found to hold calibration very well. The lower detection limits for these organic vapors were on the order of 1 ppm, as determined by the first detectable peaks above baseline noise.

Airflows into the cartridge were calibrated by using a model DTM-325 dry gas meter (American Meter Company, Horsham, Pa.). Ambient temperature and atmospheric pressure were recorded. Ambient temperature was steady enough and RH was low enough (≤85%) to avoid condensation in air lines. The LC pump(s) and breathing pump were operated until a steady-state condition existed, typically 1 to 2 hours, so that consistent concentrations could be generated before introducing the test cartridge. Once the concentration(s) reached steady state, the solvents in the LC pump reservoirs were weighed. While a reservoir was being weighed, its LC pump was switched to an alternate reservoir of the same liquid to avoid upsetting the steady-state generation of vapors. Knowing the weight of solvent used and the concentration going into and out of the cartridge, a mass balance could be done as a check on calibrations. The cartridge was then quickly inserted into the aluminum holder so that vapors in the airstream could be forced through it. The test and GC software were started at this time. Data collection by the GC was usually continued until the breakthrough curve of the third component of each mixture was completed.

Model Testing with Literature Data

The first set of data examined to test the service life estimation model for mixtures was the extensive data of Yoon and Lara et al. at dry conditions. These are discussed in the Background section. They observed full breakthrough curves of single vapors and OV mixtures for single cartridges at 24 L/min airflow, 25°C, and 40% RH. The cartridges were as-received Scott Aviation Model 642-OV containing 50 g (112 cm³) of 12–20 mesh coconut-based activated carbon. They fit breakthrough curve data as ln[P/(1-P)] vs. time t to a linear form of the Reaction Kinetic equation:

\[
t = \tau + \frac{1}{k'} \ln \left( \frac{P}{1-P} \right)
\]

where in terms used in Eq. 1, \( P = C/C_\infty \). Results were reported as \( \tau \) and \( k' \). According to Eq. 1, \( \tau = W_c W/C_\infty Q \) and \( k' = k_c C_\infty /W_c \rho B \).

Lara et al. (19) supplemented these data with data for toluene/m-xylene mixtures at 36 L/min through pairs of the same cartridges. However, they reported the results as total volumetric capacities \( W_c \) (cm³/cartridge) = \( W_e W/d_t \), as
C/C₀ = 0.5 breakthrough times τ, and as 10% breakthrough times t₁₀%.

Comparisons with model estimations required experimental 10% breakthrough times t₁₀% for the Yoon data as well, and so these were calculated from reported τ and k’ using Eq. 21 with P = 0.10.

For application of the new model, the micropore volume W₀ and adsorption potential E₀ parameters were required for the carbon used in the Scott cartridges. These were obtained from a DR plot (Figure 8). Equation 1 was used to derive Wₑ/dₑ (cm³/g carbon) from τ C₀/Q/Wₑ dₑ, which is obtained from reported τ for single vapor measurements. Then from Eq. 2 a plot of ln(Wₑ/dₑ) versus [(RT/β) ln(Pₛ/P)]² gave the slope and intercept, which led to W₀ = 0.52 cm³/g and E₀ = 19.058 kJ/mol.(2)

Putting these and other cartridge, vapor, and use conditions parameters into the model yielded 10% breakthrough times. These results are compared with experimental ones in Figure 9. The data are identified by orders of elution from the cartridges determined by model values of τ. The line on the graph is the equivalence line. Standard deviation (SD) of estimates from experimental values was 27 min (relative standard deviation RSD = 8%) for 66 first and second eluting vapors with an average bias = +1.6% and a correlation coefficient of R = 0.997. Relative standard deviation of estimates for seven third and fourth eluting vapors was 34%, largely due to an average bias of −14%. There is no satisfactory explanation for this latter bias, but it is conservative for setting change-out schedules using the model. For all 73 data sets SD = 32 min, RSD = 9%, Bias = +0.1%, and R = 0.988.

The second set of literature data used for model testing was that of Swearengen and Weaver.(26,27) They reported average (of 6) 1% and 10% breakthrough times of methyl ethyl ketone (MEK), isopropyl alcohol (IPA), hexane, butyl acetate, and ethyl benzene alone and in binary mixtures at low (20% or 50% RH) and high (85% RH) humidities. The MSA respirator cartridges containing 12-20 mesh petroleum-based activated carbon were used at 40 L/min airflow in pairs, as received or for one MEK/IPA mixture with cartridges equilibrated at the test humidities.(27)

For the previous single-vapor, all-humidity model, data from these authors for dry, single-vapor experiments were used to make a DR plot and obtain micropore volume W₀ = 0.606 cm³/g and adsorption potential E₀ = 18.70 kJ/mol.(2) Also, W₀ = 0.506 cm³/g (not the typographical error 0.560) was assumed for the denser carbon (presumably used at the AR/85% RH condition) and βₑ H₂O = 0.06 for the water affinity coefficient. These same parameters have been used for the following binary mixture estimates and comparisons.

Figures 10 and 11 show comparisons of model-calculated single vapor and mixture components’ 1% breakthrough times with experimental ones at dry and high humidity conditions, respectively. Differences (n = 16 each) from the experimental values for the dry and humid mixtures yielded (SD = 11 min, RSD = 15%, Bias = +17%, and R = 0.944) and (SD = 15 min, RSD = 32%, Bias = +13%, and R = 0.867), respectively.

FIGURE 8. Dubinin-Radushkevich plot for Yoon, Lara et al.(16−19) single vapor data for acetone, m-xylene, styrene, and toluene.

FIGURE 9. Model-calculated 10% breakthrough times vs. experimental ones for all binary, ternary, and quaternary mixtures from the work of Yoon, Lara et al.(16−19) The line is the equivalence line.

FIGURE 10. Comparisons of model-calculated single vapor and mixture components’ 1% breakthrough times with experimental ones at dry conditions from the work of Swearengen and Weaver(26,27)
The third set of literature data analyzed was that of Cohen et al.\(^{(28)}\) with binary mixtures of carbon tetrachloride and hexane or pyridine at 50% RH. They reported 10% breakthrough times corrected to 1000 ppm for both MSA cartridges and respirator cartridge tubes. For model calculations for mixtures, the carbon parameters \(W_o = 0.75 \text{ cm}^3/\text{g}\) and \(E_o = 14.78 \text{ kJ/mol}\) developed previously were used.\(^{(2)}\) Figure 12 shows the comparison of model-calculated 10% breakthrough times with experimental ones. The differences of estimates from experimental values (\(n = 18\)) yielded SD = 20 min, RSD = 21%, Bias = −0.5% and \(R = 0.970.\)

Model Testing with New Data

Experimental studies were done with two ternary mixtures to supplement the existing data and to test the multivapor model at high humidities. Figures 13 and 14 show examples of raw data breakthrough curves with measurements at 3-min intervals. In the first case (Experiment 12 in Table I), the mixture consisted of approximately 360 ppm each of acetone, trichloroethylene, and m-xylene at 80% RH and about 36 L/min cyclic airflow. The gap at about 67–81 min was due to a brief pause in the experiment to refill the LC pumps’ supplies.

Data scatter increased as the cartridge approached saturation in each vapor. At these points, breakthrough concentrations become very sensitive to slight variations in concentrations and cycling flow rate of the incoming vapors. This scatter demonstrates the responsiveness of the gas chromatographic analysis. At the important regions, less than 50% breakthrough, the breakthrough curves are smooth, which permits breakthrough times to be obtained reliably.

Figure 14 is for Experiment 17 (Table I) with approximately 280 ppm each of cyclohexane, methyl isobutyl ketone (MIBK), and toluene at 75% RH and about 36 L/min. Unlike in Figure 13 the latter two vapors were co-eluting but at differing rates. Striking features of these graphs are the rollups of the first and second eluting vapors, where breakthrough concentrations temporarily exceeded the incoming concentrations until the cartridge was completely saturated with all three vapors.
TABLE I. Experimental and Model Near 10% Breakthrough Times with Experimental Parameters for Ternary Mixtures at High Humidities

| Exp # | Vapor Observed | t_b Meas (min) | t_b Calc (min) | Breakthrough Fraction C/C_o | Avg. Conc. \( (C_a) \) (ppm) | Avg. Conc. \( (C_w) \) (ppm) | Avg. Conc. \( (C_n) \) (ppm) | T (°C) | P (atm) | RH % | Flow Rate Q (L/min) |
|-------|----------------|---------------|---------------|-----------------------------|----------------------------|----------------------------|----------------------------|--------|----------|-------|---------------------|
| 8     | Acetone        | 86.3          | 53.7          | 0.986                       | 322.1                     | 322.1                     | 322.1                     |        |          |       |                     |
| 8     | TCE            | 287.1         | 287.1         | 0.999                       | 272.1                     | 272.1                     | 272.1                     |        |          |       |                     |
| 8     | Toluene        | 674.6         | 674.6         | 0.112                       | 177.6                     | 177.6                     | 177.6                     |        |          |       |                     |
| 8     | MIBK           | 64.6          | 64.6          | 0.093                       | 325.3                     | 325.3                     | 325.3                     |        |          |       |                     |
| 11    | Acetone        | 152.1         | 152.1         | 0.114                       | 361.5                     | 361.5                     | 361.5                     |        |          |       |                     |
| 11    | TCE            | 81.1          | 81.1          | 0.099                       | 322.1                     | 322.1                     | 322.1                     |        |          |       |                     |
| 11    | Toluene        | 210.2         | 210.2         | 0.095                       | 322.1                     | 322.1                     | 322.1                     |        |          |       |                     |
| 11    | MIBK           | 55.8          | 55.8          | 0.010                       | 505.4                     | 505.4                     | 505.4                     |        |          |       |                     |
| 11    | Acetone        | 117.8         | 117.8         | 0.077                       | 505.4                     | 505.4                     | 505.4                     |        |          |       |                     |
| 11    | TCE            | 310.1         | 310.1         | 0.171                       | 505.4                     | 505.4                     | 505.4                     |        |          |       |                     |
| 11    | Toluene        | 49.1          | 49.1          | 0.056                       | 505.4                     | 505.4                     | 505.4                     |        |          |       |                     |
| 11    | Acetone        | 61.0          | 61.0          | 0.126                       | 356.0                     | 356.0                     | 356.0                     |        |          |       |                     |

Note: TCE = trichloroethylene; MIBK = methyl isobutyl ketone.

Breakthrough curves and times with single vapors were measured to establish carbon parameters. Figure 15 shows the DR plot from 26 measurements with six different vapors at dry conditions. Sampling times nearest midpoints of the breakthrough curves were interpolated to calculate the equilibrium times \( \tau \) and capacities \( W_c \). Cumulative averages (trapezoidal time integration from exposure starting times) of concentrations measured at 3-min intervals were used for partial pressures \( p_i \). The tight scatter around a straight line confirms the quality of the experiments. The linear least-squares, best-fit line shown on the graph yielded slope and intercept corresponding to adsorption potential \( E_a = 15.863 \text{ kJ/mol} \) and micropore volume \( W_o = 0.783 \text{ cm}^3/\text{g} \), respectively. From thirteen high humidity (75–91% RH) single-vapor experiments with four low-solubility vapors, an average water affinity coefficient of \( \beta = 0.06 \) was obtained with a standard deviation of 0.02.

FIGURE 15. Dubinin-Radushkevich plot for the 3M 7251 cartridge obtained by breakthrough studies with six single vapors at dry conditions.
Using these carbon parameters with cartridge parameters, vapor parameters, and test conditions, breakthrough times for mixture components were calculated using the model described above. Experimental challenge concentrations measured for each vapor at 3-min intervals were integrated using trapezoidal approximation from zero time to get cumulative concentrations. Measured breakthrough concentrations nearest 10% of these cumulative concentrations were used to get C/Co values for use in the calculations. Breakthroughs of 10% were assumed for covapors; this fraction is arbitrary, but necessary for the model calculations.

Figures 16 and 17 and Table I show 32 comparisons of the model-calculated breakthrough times versus measured times (nearest 10% breakthrough) for the two ternary vapor combinations at the humidities shown in Table I over the range of 45–89% RH. Methyl isobutyl ketone and toluene often co-eluted with overlapping breakthrough curves (e.g., Figure 14). Graphed points clustering around the equivalence lines show good agreements with SD = 22 min, RSD = 25%, Bias = −5%, and R = 0.984. Acetone estimates were generally low (conservative), possibly due to its high water solubility (completely miscible), which may not be sufficiently accounted for by the model, and/or possibly due to reactivity with water (hydrolysis, perhaps catalyzed by the carbon). Excluding acetone, the differences of estimates from 26 measurements of the other five vapors at 45–89% RH yielded SD = 21 min, RSD = 15%, Bias = +4%, and R = 0.989.

CONCLUSIONS

The good agreements of model predictions with experimental breakthrough times at dry conditions (Figures 9, 10, 12) and at humid conditions (Figures 11, 16, 17) demonstrate that the model gives reasonably good estimates for establishing service lives. Breakthrough times of all components of the mixtures (except acetone at high humidities, as explained above) were successfully predicted at all humidity levels. This included co-eluting vapors. Both experimental and model errors contribute to any differences.

As in the previous single-vapor models, the carbon parameters (micropore volume, adsorption potential, and water affinity coefficient) must be known or established from single-vapor experimental data. Ideally, they would be available from carbon and respirator cartridge manufacturers, along with cartridge parameters (carbon bed depth, diameter, effective granule size and number of cartridges on a respirator).

For the model calculations and comparisons presented in this article, the multivapor model has been implemented as a spreadsheet (initially) and as a Microsoft Visual Basic program. Both required iterations of rollups of vapor concentrations and relative humidities to converge to breakthrough time results. This is very tedious in a spreadsheet and was used in this paper only for dry conditions. However, with the computer program, the iterations were handled automatically and answers obtained quickly for both humid and dry conditions.

Properly implemented, this multivapor model can give results for one vapor as well as for more. Therefore, it can be a replacement, as well as an extension, of the single-vapor, all-humidity model and program.(2,8) Gases, which are removed by reaction instead of by micropore condensation, must be handled differently.(3)

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