1D metallic states at 2D transition metal dichalcogenide semiconductor heterojunctions

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Two-dimensional (2D) lateral heterojunctions between different transition metal dichalcogenides (TMDCs) have been realized in recent years. Homogeneous semiconducting TMDC layers are characterized by a topological invariant, their in-plane electric polarization. It suggests the possibility of one-dimensional (1D) metallic states at heterojunctions where the value of the invariant changes. We study such lateral 2D TMDC junctions by means of first-principles calculations and show that 1D metallic states emerge even in cases where the different materials are joined epitaxially. We find that the metallicity does not depend on structural details, but, as the invariant is protected by spatial symmetry only, it can be upset by breaking the symmetry. Indeed, 1D charge- and spin-density wave instabilities appear spontaneously, making 2D TMDC heterojunctions ideal systems for studying 1D systems. npj 2D Materials and Applications (2021)5:43; https://doi.org/10.1038/s41699-021-00224-1

INTRODUCTION

Lateral structures that are grown from two-dimensional (2D) materials arouse growing scientific attention, because of their potential to open a route towards truly 2D electronics. In-plane p-n junctions and barrierless Schottky contacts between 2D compounds provide the basic building blocks of 2D electronic devices1–3. Lateral heterojunctions between a variety of 2D semiconductors are realized since chemical vapor deposition techniques have enabled the growth of sharp one-dimensional (1D) interfaces between different 2D materials. Transition metal dichalcogenides (TMDCs) are a particularly versatile class of compounds, where 2D heterostructures of TMDCs with a similar crystal structure are grown routinely now4–6. 2D junctions between TMDCs with different crystal structures can also be produced7, and even structures with a large lattice constant mismatch, such as graphene or h-BN and MoS2, have been grown as lateral junctions8.

2D TMDCs, MX2, with M a (transition) metal and X = S, Se, and Te, constitute an extensive family of compounds, covering (semi) metals and semiconductors, depending on their elemental composition and their crystal phase. The compounds with M = Mo, W and X = S, Se have attracted the most attention, as they are direct bandgap semiconductors with potential applications in optoelectronics, photovoltaics, and photocatalysis9–11. Not surprisingly then, so far the focus has been mainly on junctions made from these materials, their band alignments, and interface transport properties1–4.

What has been exploited much less is the notion that, in their most common structure, these semiconductors are materials that can be characterized by an interesting topological invariant, that is, their in-plane electric polarization12–15. Insulating or semiconducting TMDCs with transition metals from different elemental groups can have a different value for this invariant. Following the general topological arguments, this suggests that if one creates an in-plane heterostructure between two such TMDCs, then at the junction the bandgap closes, and a one-dimensional (1D) metallic state is formed at the junction. This reasoning should hold for any edge or junction that involves a sudden change in invariant. Indeed, TMDC grain boundaries and edges are known to have 1D metallic states that are exclusively localized at the boundary or edge, which display electronic properties that are especially prominent in 1D systems, such as charge-density waves (CDWs), spin-density waves (SDWs), or Luttinger liquid behavior16–23. As grain boundaries and edges constitute 1D extended defects, one might argue that the appearance of 1D states is necessarily connected to the rather drastic character of these defects.

However, the presence or absence of 1D states is dictated by the change in topological invariant, the bulk polarization, of the corresponding TMDCs. In this paper, we will show that they also appear in perfectly lattice-matched heterojunctions, and these states arise out of a difference in the bulk polarization at the junction. We will discuss examples from two different cases, a polar/polar junction and a polar/nonpolar junction. The topological invariant is protected by spatial symmetry, which means it can be upset by breaking symmetry. The latter can, for instance, happen through CDWs and SDWs leading to a charge ordering and/or spin ordering with increased periodicity, which frequently is accompanied by the emergence of a (small) bandgap.

There have been computational studies on interfaces of semiconducting polar 2D materials such as AlN or ZnO, SiC, and (functionalized) graphene/BN12,24,25, where these junctions have been found to be metallic. The junction between blue and black phosphorene has been predicted to have a CDW arising at the 1D metallic interface26. However, such junctions have not been produced yet, and indeed clean junctions between these materials may be difficult to realize experimentally. Considering the recent developments cited above, in particular in controlled growth techniques, junctions between TMDCs are experimentally much more accessible.

RESULTS

Origin of the interface states

The macroscopic polarization is a topological invariant for 2D insulators with D3h symmetry15. All semiconducting TMDCs that have the H structure belong to this class. Following the modern
where \( (a, \beta) \) has the value \((2/3, 1/3)\); \( e \) is the elementary charge, and \( Q \) is the unit cell area. Choosing compounds for the junction from this group, for example, a heterojunction between MoS\(_2\) and WSe\(_2\), means that the polarization is continuous across the interface, which results in a trivial, that is, semiconducting interface. Several experiments and ab initio calculations have indeed confirmed that this junction is semiconducting with a type-II (staggered) band alignment\(^{13}\).

### Polar/polar TMDC junctions

The group V TMDCs MX\(_2\) (M = V, Nb, Ta; X = S, Se, Te) all are metallic, which is due to the transition metals having one less valence electron compared to group VI transition metals. Group IV TMDCs in the H structure, such as TiS\(_2\), are again semiconducting, with a calculated polarization \( P \) with \((a, \beta) = (1/3, 2/3)\) that is different from that of group VI MX\(_2\). As this means that the topological invariant of group IV TMDCs is different from that of group VI TMDCs, this suggests the possibility of creating a nontrivial, that is, a metallic junction between, for instance, TiS\(_2\) and MX\(_2\). The T structure of TiS\(_2\) is actually lower in energy than the H structure, and is not suitable, as it is metallic. However, we suggest that it may be possible to create the metastable TiS\(_2\) H structure by a suitable choice of growth conditions, as likewise, it is possible to create the metastable metallic T structure of MoS\(_2\) by suitable growth conditions\(^{10}\).

To be specific, an H-TiS\(_2\) monolayer has a calculated optimized lattice constant of 3.34 Å, which is within 1% of the optimized lattice constant of 3.31 Å of MoSe\(_2\). Both compounds are semiconductors, with TiS\(_2\) having a calculated (indirect) bandgap of 0.7 eV and MoSe\(_2\) having a (direct) bandgap of 1.6 eV. These two semiconductors form a type-II band alignment according to our density functional theory (DFT) calculations, which, apart from the topological considerations discussed above, would result in a semiconducting junction.

Figure 1a shows our supercell model for the TiS\(_2\)/MoSe\(_2\) junction along the zigzag direction. There are two different junctions in the supercell, due to the periodic boundary conditions imposed in the calculations. We call these the Ti edge and Mo edge, respectively, according to the transition metal atoms closest to the junction. Choosing a stoichiometric Se-S termination at the interfaces, as shown in the figure, we optimize the lattice constants again over the whole structure. After relaxation, the original bond lengths and angles are actually retained, and the structure has a uniform lattice constant close to 3.34 Å.

Figure 1b shows the calculated non-spin-polarized bands of this structure, using a 1× periodicity in the direction of the Mo and Ti edges. There is a clear bandgap, with two bands crossing the gap. The wave functions associated with these two bands are localized at the two junctions in the supercell, where one band can be assigned to the Ti edge and the other to the Mo edge. The two edges clearly are metallic, with the Ti edge band being 1/3 occupied and the Mo edge band being 2/3 occupied.

The Mo edge state has dominant Mo \( d_{xy} \) and \( d_{z^2} \) character, see Fig. 1c, whereas the Ti edge state has foremost Ti \( d_{xy} \) and \( d_{xz} / d_{yz} \) character, with some participation of the other metal atom’s \( d \) states, see Fig. 1d. As the chalcogen atoms do not contribute appreciably to these edge states, this would imply that changing the chalcogen atoms at the edges would not affect the electronic structure. Indeed, on changing the chalcogen terminations at the junctions from a stoichiometric S-Se to a nonstoichiometric Se-Se or S-S, no change in the occupation or the dispersion of the edge states is observed.

Both the existence of states localized at the junctions, with energies in the bandgap, as well as the occupancy of those states can be deduced from the 2D polarization of the materials involved and its topological character. Going from material 1 to material 2 across a junction, the polarization jumps from \( P_1 \) to \( P_2 \), which...
would result in a polarization line charge density at the junction $\lambda = (P_2 - P_1) \cdot n$, where $n$ is the in-plane unit vector normal to the junction. For a macroscopic junction, this polarization charge has to be neutralized by a compensating line charge density of the same sign, such as to avoid an intrinsic electric field generating a polar catastrophe.$^{21,31,32}$

In the present case, the compensating charge can only be of electronic origin and resides in states near the Fermi level, inside the bandgap. Following the reasoning of topological invariants, going across a junction from an insulator with a certain value for the topological invariant to an insulator with a different value for that invariant, then at the junction the gap has to close, that is, the junction is metallic, where the metallicity is carried by states localized at the junction.

Going from MoSe$_2$ to TiS$_2$, this gives $\lambda = (2e)/(3a)$ at the Mo edge, where $a$ is the lattice constant along the edge, which means that the corresponding edge state has to be 1/3 occupied by holes (taking spin degeneracy into account). At the Ti edge, going from TiS$_2$ to MoSe$_2$, we have $\lambda = -(2e)/(3a)$, and an edge state that is 1/3 occupied by electrons.

This interpretation is in line with the three-dimensional case of junctions between insulating oxide perovskites, such as LaAlO$_3$/SrTiO$_3$, where a 2DEG emerges at the interface between the two insulators.$^{33}$ The interface metallicity has been attributed to the abrupt change of the valence charge of the cation at the interface, from La$^{3+}$ to Ti$^{4+}$, causing a charge transfer of 0.5e in order to avoid a polar catastrophe. The 2D heterojunction between AlN and SiC has been analyzed in similar terms, where the difference in formal charges between the cations and anions in the 2D III–V and the IV–IV materials drives the formation of a 1DEG at the interface, in order to avoid a polar catastrophe.$^{25}$

Our TMDC case is more subtle because there is no ionic charge discontinuity at the interface. The formal charges on the cations and ions on both sides of the junctions are the same in their respective compounds, Ti$^{4+}$(S$^{-2-}$)$_2$ and Mo$^{4+}$(Se$^{-2-}$)$_2$. Moreover, the compounds have the same structure, and we also see no structural distortions at the junction. The difference in polarization between the two compounds is then of purely electronic origin, as is the metallicity of the junction.

Formally, the analysis of the metallic junction presented above only holds in the macroscopic limit, that is, in the case where one has one junction between two semi-infinite 2D materials. Nevertheless, in our supercell model, which comprises strips of six TMDC units wide, we apparently already have reached this asymptotic limit. We found that if one uses strips of four or fewer units, one still observes edge states, see Supplementary Fig. 3, but the edge states at the Mo and Ti edges interact across the strip. This causes a gap to open up, similar to hybridization between orbitals resulting in a latticebending splitting, which is used to describe chemical bonding.

We see no evidence for a residual electric field existing over the width of the ribbon. The electrostatic potential is approximately constant over the TiS$_2$ and the MoSe$_2$ regions and has a step at the interface, see Supplementary Fig. 1. The electrons residing in the edge states have then fully compensated the polarization charge. This is in agreement with an earlier work that shows that an electric field is present only if there are no edge states to compensate for the differences in polarization.$^{35}$ The band structure and the dispersion of the edge states suggest that the latter are not bulk states driven up or down by an electric field, but new states created in the gap.$^{35}$

**Polar/nonpolar TMDC junctions**

The T-phase structure of TMDCs has zero polarization because it has inversion symmetry. Most of the T-phase TMDCs are metallic compounds, but HfS$_2$ and HfSe$_2$ are semiconductors. Constructing a junction between one of these and a semiconducting H-phase TMDC gives a topological discontinuity, which results in a metallic junction similar to that described in the previous section. The calculated lattice constant of T-HfS$_2$ is 3.62 Å, which is close to that of H-MoTe$_2$, 3.56 Å, implying that a heterojunction between the two can be formed with minimal strain. The Perdew–Burke–Ernzerhof (PBE) bandgaps of T-HfS$_2$ and H-MoTe$_2$ are 1.3 and 1.1 eV, respectively, and the band alignment between the two is type II, which, apart from polarization considerations, would imply a semiconducting junction. T–H junctions cannot be stitched perfectly, with all metal atoms at the junctions having sixfold coordination by chalcogen atoms. In experimental work, one finds the $\delta$-junction structure$^{25,34}$, where the metal atom on the T side of the junction (the Hf atom in this case) has sevenfold coordination, and the atom on the H side (the Mo atom) has sixfold coordination. We adopt this structure at one interface, calling it the Hf edge in the following. At the other interface, called the Mo edge, we construct a similar structure, giving the Hf atom a sixfold and the Mo atom a sevenfold coordination. Figure 2a shows the unit cell, where the two junctions are marked. More detailed images of the edge structures are given in Supplementary Fig. 4.

On optimizing, the lattice constant for the whole structure becomes 3.60 Å. The bond lengths involving atoms close to the interface undergo changes, while the atoms far away from the interface in both the H and T phase remain at their respective bulk positions.

The coordination at the edges does not influence the bulk polarization, of course. It also does not affect the fractional character of the polarization charges at the edges, as by adding or removing an atom one simply adds or removes an integer number of electrons. Therefore, edge metallicity is robust against atomic defects at the junction. To test this, we have also constructed a Mo edge structure where the Hf atom has a fivefold coordination and the Mo atom has a sixfold coordination, which gives a very similar electronic structure. Details can be found in Supplementary Fig. 5.
The electronic structure of H-MoTe$_2$/T-HfS$_2$ heterojunctions is shown in Fig. 2b. It clearly displays a bandgap, with two bands, localized at the junctions, crossing in the gap at the Fermi level. The band from the Hf edge (β-junction) is 2/3 occupied, and its character is a combination of Mo and Hf $d_{xy}$ and $d_{yz}$ orbitals, Fig. 2c. At the Mo edge, the band is 1/3 occupied and has predominant Mo $d_{xy}$ and $d_{yz}$ character, see Fig. 2d. The existence of these localized states and their occupancy follows from similar considerations as for the H–H junctions discussed in the previous section.

### 1D electronic instabilities

The metallic states at TMDC junctions clearly have a 1D character. Electron correlation and electron–lattice interactions are particularly effective in 1D systems and can perturb the metallic character. In the present case, the 1D states have an occupancy of 1/3 or 2/3, which suggests the possibility of a CDW and/or an SDW that triples the period in the direction along the junction. This would be similar to the edges of a TMDC SDW, creating gaps of 0.45/0.22 eV, respectively. The PBE functional, both after structural relaxation. The latter gives an FM/AFM SDWs at the Mo/Ti interface. An antiferromagnetic arrangement is 60 meV/3× modulation is largest at the Mo edge, with distances between the Mo atoms of 3.27 and 3.41 Å, whereas the distances between the Ti atoms at the Mo edge do not change much. At the Ti edge, the distances between Ti atoms are 3.29 and 3.33 Å, and there are no significant changes in the bond distances between the Mo atoms.

The SDW/CDWs lead to a metal–insulator transition, resulting in a bandgap in both the spin configurations (Fig. 3b). The bandgap at the Mo edge is 0.45 eV, whereas at the Ti edge, it is 0.22 eV. The SDW/CDWs lower the total energy by 330 meV/3× cell compared to the undistorted structure. The exact value of $U - J$ is not too critical for the emergence of an SDW/CDW and a gap. The SDW/CDW persists for values of $U - J$ in the range 2–3 eV, although the magnetic moments and the bandgap decrease on decreasing $U - J$, see Supplementary Fig. 2. The correlation-driven SDW/CDWs seem to be a unique feature of 2D TMDC junctions, due to the presence of $d$ electrons on the transition metals. In the AlN–SiC case, where $d$ electrons are absent, spin-polarized DFT calculations do not give SDW/CDWs, and the junctions remain metallic.

In the case of the H-MoTe$_2$/T-HfS$_2$ junction, simply optimizing the 3× structure with the PBE functional gives a distinct CDW with a clear 3× modulation of the structure at both the junctions. The modulation is largest at the Mo edge, with distances between the Mo atoms at the edge becoming 3.39 and 4.11 Å. At the Hf edge, the modulation is somewhat smaller, with distances between the structure of the 3× structure. Although the electronic structure close to the Fermi level looks complicated, with multiple bands crossing, these bands are actually the same as the ones shown in Fig. 1b, but folded because of the 3× periodicity. The Mo edge band, which is 2/3 occupied in the 1× cell, is then folded into three bands, with the two lower bands fully occupied, and the topmost one fully empty. The Ti edge band, 1/3 occupied in the 1× cell, is folded similarly, with the lowest band fully occupied, and the two upper ones fully empty.

The metallic edge bands in Fig. 3a display the prototypical 1D band structure that is susceptible to perturbations inducing a metal–insulator transition, such as a Peierls distortion, or a CDW/SDW, but a DFT calculation using the PBE functional does not find any of these. The 1D states have mostly Mo $d$ character, and although the on-site electron–electron Coulomb interaction in 4d transition metals is weaker than in 3d ones, it is not always negligible. In previous calculations on mirror twin boundaries of MoSe$_2$, we have found that the inclusion of on-site Coulomb and exchange interactions as in the PBE + U mean-field approach markedly changes the electronic structure of the 1D states. Therefore, we repeat the calculations in the 3× cells, using the PBE + U functional with $U - J = 3$ eV for the Mo 4$d$ electrons. In principle, one can also include such a parameter for the Ti 3$d$ electrons, but this has little effect, as in TiS$_2$ these states are mostly empty. The top of the TiS$_2$ valence band has sulfur $p$ character, and the Ti 3$d$ states only contribute significantly to the conduction band. We have also tested values of $U - J$ over the whole range 0–3 eV; details can be found in Supplementary Fig. 2. The PBE + U functional indeed gives rise to the opening of a bandgap in the band structure, as shown in Fig. 3b. It is caused by SDWs at both the Mo and Ti edge junctions. In these SDWs, the Mo atoms closest to the junctions carry a magnetic moment, whereas the Ti atoms at the junctions, and the atoms further away from the junctions, do not show any magnetic moments. Several (meta)stable magnetic configurations of Mo atoms at the two interfaces are found. The configuration with the lowest total energy has a ferromagnetic arrangement at the Mo edge, with magnetic moments of 1.0, 1.0, and 0.0 $\mu_B$ on the three Mo atoms at the junction. An antiferromagnetic arrangement is 60 meV/3× cell higher in energy. At the Ti edge, we found the AFM arrangement to be the lowest in energy, with magnetic moments on the three Mo atoms at the junction of $-1.0, +0.6$, and $+0.6 \mu_B$.

The SDWs are accompanied by CDWs and (slight) distortions of the structure at the junctions. The Mo atoms at the Mo edge adopt a 3× periodicity, with distances between the Mo atoms of 3.27 and 3.41 Å, whereas the distances between the Ti atoms at the Mo edge do not change much. At the Ti edge, the distances between Ti atoms are 3.29 and 3.33 Å, and there are no significant changes in the bond distances between the Mo atoms.

### Fig. 3

The band structure of the H-MoSe$_2$ and H-TiS$_2$ heterojunction calculated in the 3× supercells. The states highlighted in blue and red belong to Mo and Ti edges, respectively. a Calculated with the PBE functional, b with the PBE + U functional, both after structural relaxation. The latter gives an FM/AFM SDWs at the Mo/Ti edges, creating gaps of 0.45/0.22 eV, respectively. c Spin-density wave at the Mo edge and d at the Ti edge; the red/green colors indicate spin up/down, where the SDWs result in the three Mo atoms at the junction becoming inequivalent.
Hf atoms at the edge becoming 3.54 and 3.69 Å. These Peierls distortions open up a gap of 0.6 eV at the Mo edge and 0.15 eV at the Hf edge, and lower the energy by 270 meV/3× cell. The band structures of the undistorted and the distorted structures are shown in Fig. 4. Adding spin polarization has no effect, but upon adding on-site interactions, with $U - J = 1.5$ eV, magnetic moments of $-0.48$, $0.54$, and $-0.30 \mu_B$ develop on the Mo atoms at the Mo edge, whereas the Hf edge remains unpolarized. The bandgaps change only slightly upon adding $U$ at the Mo edge, it is 0.17 eV, and at the Mo edge, it is 0.42 eV, see Supplementary Fig. 6 for the corresponding band structures.

DISCUSSION
We have shown by means of first-principles DFT calculations that lateral heterojunctions of 2D semiconducting TMDCs can have 1D metallic in a 1× unit cell. The metallicity arises out of a discontinuous topological invariant at the junction, the in-plane electric polarization, which is nonzero for TMDCs in the H structure. Such heterojunctions can be made from two semiconducting TMDCs, both in the H phase, with different values for the topological invariant, and matching lattice constants. Alternatively, junctions can be made between a TMDC in the H structure with nonzero polarization and one in the T structure with zero polarization, again with matching lattice constants. Changing the chalcogen atoms or creating defects at the junctions will not affect the invariant and hence metallicity is preserved.

The 1D metallic states are, however, susceptible to the instabilities of 1D metals originating from electron–electron and electron–lattice interactions. Using DFT + U calculations, we show that spin- and/or charge-density waves create a bandgap at the junction, which is, however, much smaller than the bandgaps of the two TMDC semiconductors. The details of these density waves depend upon the detailed structure of the junction. We propose that 2D TMDC heterojunctions are ideal systems for studying 1D physics.

METHODS
Density functional theory
To model a 2D TDMC heterojunction, we build a supercell that has a width of twelve MX₂ unit cells, six for each of the two compounds forming the junction. This unit is periodically repeated in plane, such that each supercell contains two junctions, see, for instance, Fig. 1a. Perpendicular to this 2D plane, we use a vacuum spacing of 15 Å to prevent an interaction between the periodic images.

We perform DFT calculations, with the generalized gradient approximation PBE and PBE + U functionals, and the projector augmented wave method, using the Vienna ab initio simulation package (VASP). For the transition metals in MX₂, the outer s, p, and d shells are treated as valence electrons, and for the chalcogen atoms, the outer s and p shells. A cut-off of 400 eV for the kinetic energy of the plane waves and a k-point sampling of 12 points per unit cell along the direction of the junction are used. All atomic positions along with the lattice constants are relaxed, till the forces on the atoms are < 0.05 eV/A, with a total energy convergence criterion of $10^{-5}$ eV.

For the PBE + U calculations, we use the rotationally averaged formulation, as implemented in VASP, which applies a single parameter $U - J$⁴. We use a value $U - J = 3$ eV, which is appropriate for 4d transition metals, and test values between 0 and 3 eV⁴⁴⁻⁴⁶.

DATA AVAILABILITY
The authors declare that all data supporting the findings of this study are available within the paper and its Supplementary information files.

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AUTHOR CONTRIBUTIONS
G.B. conceived the idea and S.K. performed the DFT calculations. Both authors were involved in discussing the results and in writing the manuscript.

COMPETING INTERESTS
The authors declare no competing interests.

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