What can we learn from Dijet suppression at RHIC?

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We present a systematic study of the dijet suppression at RHIC using the VNI/BMS parton cascade. We examine the modification of the dijet asymmetry $A_j$ and the within-cone transverse energy distribution (jet-shape) along with partonic fragmentation distributions $z$ and $j_l$ in terms of: $\hat{q}$; the path length of leading and sub-leading jets; cuts on the jet energy distributions; jet cone angle and the jet-medium interaction mechanism. We find that $A_j$ is most sensitive to $\hat{q}$ and relatively insensitive to the nature of the jet-medium interaction mechanism. The jet profile is dominated by $\hat{q}$ and the nature of the interaction mechanism. The partonic fragmentation distributions clearly show the jet modification and differentiate between elastic and radiative+elastic modes.

I. INTRODUCTION

Recent measurements showing the strong modification of high energy $E_t \sim 100 – 200$ GeV dijets at the LHC [1,2] in Pb+Pb collisions have sparked an interest in using dijets to quantify jet modification in hot QCD matter. Proposed upgrades to the PHENIX experiment, and continuing development of jet reconstruction at STAR, promise access to dijets in a different kinematic region, $E_t \sim 15 – 65$ GeV at RHIC. The dijet asymmetry

$$A_j = \frac{E_{t,l} - E_{t,s}}{E_{t,l} + E_{t,s}}, \quad (1)$$

where $E_{t,l}$ is the transverse energy of the leading jet and $E_{t,s}$ is that of the sub-leading jet, has been successfully reproduced by various authors with a variety of models [3–6]. Recent work by Renk [7] has indicated that these results may be relatively insensitive to the fine details of jet energy loss, suggesting that $A_j$ may be unsuitable for tomographic purposes. If this is indeed the case are there other more differential dijet observables for jet measurements at RHIC?

With these issues in mind we have used the VNI/BMS parton cascade to systematically explore dijet suppression at RHIC energy scales under controlled medium conditions. We examine the modification of dijets under variation of the medium radius and temperature, the strong coupling constant and the jet definition in terms of: $\alpha_s$; the nature of the interaction mechanism. We then show results for the leading parton energy loss and discuss the modification of dijets at RHIC in terms of: the asymmetry $A_j$, the jet radial profile, and partonic fragmentation distributions $z$ and $j_l$.

II. THE PARTON CASCADE MODEL

The parton cascade model (PCM) is a Monte-Carlo implementation of the relativistic Boltzmann transport of quarks and gluons

$$p^\mu \frac{\partial}{\partial x^\mu} F_k(x,p) = \sum_i C_i F_k(x,p). \quad (2)$$

The collision term $C_i$ includes all possible $2 \rightarrow 2$ interactions and final-state radiation $1 \rightarrow n$

$$C_i F_k(x,p) = \frac{(2\pi)^4}{2S_i} \int \prod_j d\Gamma_j |M_j|^2 \times \delta^4(P_{in} - P_{out}) D(F_k(x,p)), \quad (3)$$

$d\Gamma_j$ is the Lorentz invariant phase space for the process $j$, $D$ is the collision flux factor and $S_i$ is a process dependent normalization factor. A geometric interpretation of the total cross-section is used to select pairs of partons for interaction. Between collisions, the partons propagate along straight line trajectories.

In the VNI/BMS PCM outgoing off-shell partons are brought back on-shell through a medium modified time-like branching. The partons created in this process is subject to a Monte-Carlo LPM effect, see below.

The strong coupling constant for scatterings is nominally held fixed at $\alpha_s = 0.3$ although we shall explore the effects of its variation below. A QGP medium is simulated as a box of thermal quarks and gluons generated at some fixed temperature. Periodic boundary conditions are imposed on the box, whose size is selected to be large.

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enough that if a simulated jet wraps around it will not interact with its own tail. The jet transport coefficient characterizing the amount of transverse momentum acquired by particles in transit through a perturbative thermal medium $\hat{q}$ can be analytically computed [10, 11] and also deduced from the simulation. The analytical result is

\[
\hat{q}(T) = \frac{C_R g^4}{4\pi} N(T) \ln \left( \frac{q_{\text{max}}^2(E,T)}{m_D(T)^2} + 1 \right),
\]

\[
m_D(T)^2 = \left(1 + \frac{1}{6} N_f\right) g^2 T^2,
\]

\[
N(T) = \frac{\xi(3)}{\xi(2)} \left(1 + \frac{1}{4} N_f\right) T^3,
\]

\[
q_{\text{max}}(E,T) = \sqrt{E T}.
\]

where $T$ is the medium temperature $m_D(T)$ is the Debye screening mass, $N$ is the medium density and $q_{\text{max}}$ is a cutoff resulting from the parton scattering kinematics. See Fig. 1 for a comparison of results from VNI/BMS and [4]. The partonic contents of jets created by a suitable event generator and evolved down to $Q_0 = 1$ GeV, in this study PYTHIA 8 [12, 13], are injected into the medium one at a time, they propagate for a given distance, and their evolution is recorded. The jet evolution is recorded at run-time without reference to any particular jet definition (cone-angle, energy cuts, jet reconstruction algorithm, etc). Instead each particle in the initially inserted jet is marked as being “jetty”, this jettiness tag is then iteratively applied to all partons that interact with an already jetty-labeled parton. The entire time-evolution of the jet can then be reconstructed using a suitable jet finder (FastJet [14]) and jet definition. In this way the influence of varying jet definitions can be readily studied. We emphasize that the medium partons propagate along with the jet during this process, continually interacting and mixing with the evolving jet. This medium back-reaction is a unique feature of parton cascades.

VNI/BMS is a simple enough jet-suppression model. While it may not be suitable for use as a full event generator, lacking hydrodynamical flow and hadronization, the active medium and medium-modified radiation make it a useful test bed for many but not all jet modification features. As we shall show below the effects of hadronization are rather important for certain intra-jet observables. We shall reexamine these observables in a future work with a hadronization solution implemented in the model.

III. A MONTE-CARLO LPM EFFECT

The emission of radiation in QCD is not an instantaneous process. There is a time period during which the radiated quanta and the radiator are in a correlated state. If this takes place in a dense medium the correlated wave function may interact with the medium constituents leading to a modification of the decoherence process. If the emitting parton interacts with several additional medium scattering centers then quantum interference effects lead to an in medium path-length dependence for the amount of energy radiated, this is the Landau Pomeranchuk Migdal (LPM) effect [15, 16].

The formation time of a parton with energy $E$ and time-like virtuality $Q$

\[
\tau_f = \frac{E}{Q} \approx \frac{\omega}{k_t^2},
\]

is the lifetime of this virtual correlated state and characterizes the emission process.

We implement an approximation to the full pQCD description of the interaction of the radiating system with the medium using a local Monte-Carlo routine in the style of Zapp and Wiedemann [17]. This prescription reproduces the leading BDMPS-Z [18, 19] result for light-parton energy loss in a QGP medium $\Delta E \sim L^2$. This method is particularly appealing since it requires no artificial parametrization of the radiative process, it is a purely probabilistic medium-induced modification.

In VNI/BMS a set of partons is produced by time-like branching after an inelastic scattering. The branching process evolves the initial time-like virtuality $Q$ of the outgoing parton pair downwards to a cutoff $Q_0 \approx 1$ GeV, converting virtuality into energy and transverse momentum of radiated partons. The formation time of these evolving partons [6] is computed for each intermediate stage of the branching process. The hardest gluon in the final state of the time-like branching is selected to be the probe parton.

The formation times

\[
\tau_f^0 = \sum_{\text{branchings}} \frac{\omega}{k_t^2},
\]

for all sub-branchings that occur during the time-like branching procedure leading up to the production of the
probe gluon are summed, giving the initial formation time for the probe gluon. The selection of the hardest gluon to represent the shower reflects the dominance of gluon re-scattering in QCD interference processes.

The probe parton is allowed to propagate through the medium and interact elastically with other partons in the medium. After the n-th scattering its formation time is recalculated as

\[ \tau_f^n = \frac{\omega}{(k_\perp + \sum_{i=1}^{n} q_{\perp,i})^2}. \]  

(7)

This tends to decrease the formation time relative to the original value with each additional scattering, leading to an increased energy loss rate. This simulates the emission of the shower with coherent interference from n centers. After the formation time expires, the radiation is considered to have decelerated from the initiating particles and all involved partons may interact and radiate.

The performance of this prescription has been verified by considering the energy loss of a 100 GeV jet inserted into a medium at fixed temperature \( T = 0.35 \) GeV, see Fig. 2. The elastic energy loss in the VNI/BMS parton cascade has been previously shown to agree well with perturbative calculations [11]. The measured radiative energy loss is well described by BDMPS-Z [18] which gives,

\[ -\Delta E = \frac{\alpha_s C_R \mu^2}{8 \lambda_g} L^2 \log \frac{L}{\lambda_g}. \]  

(8)

By fitting the radiation only curve (the blue open squares in Fig. 2) with this functional form we match the leading coefficient to within 20%.

The elastic energy loss process is dominant for short times since the average formation time arising from the first hard collision of the leading-parton with the medium is \( \langle \tau_f \rangle \sim 5 \text{ fm/c} \). This leads to the initial suppression of the radiative process as we have required that no energy be lost from the radiating parton until the formation times of the radiated quanta have expired.

IV. RESULTS

We generated candidate dijet events from Monte-Carlo pp collisions at \( \sqrt{s} = 200 \) GeV using PYTHIA 8. Anti-kt reconstruction was used to identify satisfactory dijet events [20]. The following kinematic requirements were always imposed: \( p_{t,\text{min}} = 5 \) GeV, \( \Delta \eta_{12} < 1.1 \), \( \Delta \phi_{12} > \pi/2 \) where \( \Delta \eta_{12} \) and \( \Delta \phi_{12} \) are measured between the two reconstructed jets in the event. The constituent partons of each identified jet were translated from PYTHIA into the parton cascade medium for modification. The two jets in each event are evolved separately. Table I shows the ranges of each parameter we included in the study. The study contains a total of 16000 dijet events for each combination of parameters. For a given medium radius \( R_{med} \) we generate dijet path lengths by uniformly sampling \( 2d \) jet vertices within a circle of radius \( R_{med} \) and then generating a chord with a uniform angular distribution. The two chord segments define the path lengths for the dijet pair. The leading jet is defined as the jet with the highest energy at the point of observation, the leading jet from the vacuum event may not be the leading jet after medium evolution.

We consider the dijet asymmetry \( A_J \), the partonic jet radial profile and the partonic distribution of energy within the jet in terms of the variables \( z = p_t/E_t \cos(\Delta r) \) and \( j_t = p_t \sin(\Delta r) \), where \( p_t \) is the transverse momentum of a parton within the jet, \( E_t \) is the total transverse momentum of the jet and \( \Delta r = \sqrt{\Delta \eta^2 + \Delta \phi^2} \) is the angle between this parton and the jet axis.

We have previously applied VNI/BMS [5] with a static medium to jets at LHC scales \( \sqrt{s} = 2.76 \) ATeV, see Fig. 3. Here we followed the dijet kinematics as described by CMS [2], \( E_{t,J} > 120 \) GeV, \( E_{t,s} > 50 \) GeV and \( \Delta \phi_{12} > 2\pi/3 \). A Gaussian smearing was applied to reconstructed jet energies to approximate detector response. In this case a medium with \( T = 350 \) MeV and \( R_{med} = 3 \) fm gives a relatively good fit to the CMS results [2]. This suggests that VNI/BMS can produce reasonable jet modification. Given the complexity of the actual de-
In Fig. 4 we show the variation of asymmetry under variation of all the factors in our definition of leading jets that travel a very long distance and so experience a short distance, and are less modified, along with sub-leading jets which travel a few fm and lose no energy. The sub-leading contribution to the observed asymmetry is relatively insensitive to this parameter. We explore the variation of the strong coupling constant \( \alpha_s \) in Fig. 3. The strength of elastic interactions are scales with the strong coupling and so \( \tilde{q} \propto \alpha_s^2 \). The radiative process itself also depends upon the strong coupling, the total cross section for emission in the DLA (double log approximation) scheme is \( \sigma_N \propto (g_s^2 \log q)^N \) where the large logs arise from the kinematics of small angle radiation \([21]\). Given these considerations it is interesting to note that the relative similarity of the results with and without radiation.

Let us now examine the modification of the radial jet profile under the same set of factors. We define the radial jet profile as the ratio of jet energy reconstructed within a certain jet-cone radius \( R \) relative to the reconstructed energy at \( R = 1 \). This gives a normalized radial profile which is very sensitive to variations in the medium temper-
FIG. 4: The dijet asymmetry as a function of the path length of the leading and sub-leading jets, for a medium with $T = 250$ MeV (left) and $T = 350$ MeV (right). Both figures show anti-kt reconstructed jets of radius $R = 0.2$ with $E_{t,t} \geq 20$ GeV and all events include both radiative and elastic energy loss.

FIG. 5: The joint energy loss distributions for leading and sub-leading jets at $T_{med} = 350$ MeV with $R_{med} = 5$ fm and anti-kt $R = 0.2$. The left figure shows the elastic only mode, right figure shows elastic + radiation.

FIG. 6: Showing the distribution of energy loss against path length for leading (left) and sub-leading (right) jets at $T_{med} = 350$ MeV with $R_{med} = 5$ fm and anti-kt $R = 0.2$ in the full radiation+elastic simulation.
FIG. 7: Showing the influence of the medium temperature and the jet-medium interaction mechanism for dijets with \( E_{t1} \geq 20 \text{ GeV} \). The left panel shows elastic scattering only, the right panel shows the full elastic and radiative process. All events are for anti-kt reconstructed jets with \( R = 0.2 \) and \( R_{med} = 5 \text{ fm} \).

FIG. 8: Showing the variation of \( A_j \) under variation of \( R \) the Anti-Kt jet cone radius, elastic only (left) and elastic + rad (right). The medium radius is kept fixed at \( R_{med} = 5 \text{ fm} \) with \( T = 0.35 \text{ GeV} \) and \( E_{t,\ell} > 20 \text{ GeV} \).
temperature, the jet interaction mechanism and the strong coupling. This observable could be experimentally obtained by a similar process of iterative jet reconstruction. In Fig.\[1\] we show the radial profile at two medium temperatures for both elastic and radiatively modified jets. The leading jet profiles (solid lines) are somewhat modified compared to the vacuum jets (black profiles), we see very little separation between the radiative and elastic only leading jet profiles. The sub-leading jet profiles are dramatically modified compared to the vacuum and leading jet profiles. At both temperatures the elastic and radiative sub-leading jet profiles clearly separate, the radiative sub-leading jets become broader and softer than the elastic only. Both sets of sub-leading jets become much broader and softer compared to the leading jets. This is in line with our observations of the energy loss distributions as shown in Fig.\[5\]. In Fig.\[2\] we show the jet profiles’ sensitivity to the strong coupling. The leading jet profiles are somewhat modified at $\alpha_s = 0.6$, the sub-leading jet profiles soften smoothly with increasing $\alpha_s$. It is interesting to note that the shape of these soft sub-leading profiles is different for elastic (left) and radiative (right) jets, the elastic profiles become increasingly convex as $\alpha_s \to 0.6$ while the radiative profiles remain concave.

Finally we examine the partonic fragmentation distributions in the longitudinal and transverse variables $j_t$ and $z$. Examining the single inclusive jet distribution at RHIC scales $\sqrt{s} = 200$ GeV and $E_t \sim 15 - 65$ GeV we find that the average partonic multiplicity in a vacuum PYTHIA jet is $\langle N_{\text{parton}} \rangle = 5.6$ which is roughly tripled during hadronization $\langle N_{\text{hadron}} \rangle = 14.6$, this hadronization process will conserve the total $E_t$ of the jet but in so doing will redistribute the components of the momentum transverse to the jet axis. This means that the partonic and $j_t$ and $z$ distributions cannot be directly compared with experiment. What may be a surprise is the observed large peak in the $z$ distribution at 1 corresponding to jets with a single parton, this is seen in the vacuum and modified jet results. This peak is a consequence of the vacuum radiation evolution which is kinematically limited at RHIC regimes. We note that at LHC jet scales $E_t \sim 50 - 300$ GeV and $\sqrt{s} = 2.76$ TeV $\langle N_{\text{parton}} \rangle = 19.5$ and $\langle N_{\text{hadron}} \rangle = 46.5$, at these scales the $z = 1$ peak vanishes.

In Fig.\[3\] we show the VNI/BMS partonic $z = p_t/E_t \cos(\Delta r)$ distributions for elastic and radiative jets alongside the vacuum results. Note the strong peak at $z = 1$ in both cases, this peak is actually enhanced by the evolution. In the elastic case this enhancement comes from a depletion of the low $z$ distribution. If a jet initially contains only one or two soft partons and a hard core the soft partons will most likely be scattered out of the jet cone. This leads to an enhancement of jets measured with $z = 1$ and a depletion of the low end of the spectrum. The same process takes place in the radiative case, the right panel of Fig.\[3\] but here the soft radiated partons tend to fill the small $z$ distribution while the mid $z$ range sees the most depletion. These middle $z$ partons interact with the medium producing a shower of soft radiation. The enhancement of the $z = 1$ peak is smaller in the radiative case than in the elastic case as these hard core partons radiate and soften the jets. As the jet cone radius is increased the peak at $z = 1$ is diminished as more of the soft scattered partons are recaptured by the jet definition this also enhances the peak at small $z$ in the radiative case, see Fig.\[14\]. The transverse $j_t = p_t \sin(\Delta r)$ distribution is shown in Fig.\[15\] for elastic and radiative jets. The evolved $j_t$ distribution is softened in both cases as interactions with the medium and radiation add more soft partons to the jet. The radiative jets have a slightly steeper profile than the elastic only jets, radiated soft partons are more strongly confined to small $j_t$.

V. CONCLUSIONS

We have examined the modification of RHIC scale di-jets by a pQCD medium over a range of temperatures and coupling constants. We find that the dijet asymmetry is quite sensitive to the amount of medium encountered by the jets, and very sensitive to variations in $q$. We do not observe a strong dependence of $A_j$ upon the jet interaction mechanism which is intriguing. The leading jets show a strong surface bias and lose very little energy making their $E_t$ a reasonable proxy for their initial energy. As such $A_j$ appears to give a reasonable measure of the modification of sub-leading jets at these scales.

The jet profiles we present show the strong modification of the sub-leading jets as a function of temperature and strong coupling. They also differentiate between interaction mechanisms, understanding the nature of the jet-medium interaction as well as its strength is of paramount import. Although these profiles may well be sensitive to the non-trivial hadronization process, we believe that they could provide a very informative window into the real nature of jet interactions with the QGP.

The fragmentation distributions provide another interesting window into jet modification. The observed structures in $z$ reveal the importance of the interplay of vacuum radiation and the fragmentation process. Although hadronization will certainly change these distributions these results already demonstrate the importance of medium induced transverse diffusion in the jet modification process.

Dijets at RHIC scales are likely to be strongly modified by the presence of the deconfined QGP medium. The observables we have discussed are sensitive to many aspects of this modification and suggest that further jet measurements at RHIC will provide valuable insights into the nature of the QGP and into the applicability of pQCD jet suppression models.
FIG. 9: The influence of applying cuts to the leading jet energy on $A_j$. The left panel shows only elastic scattering processes, the right panel shows radiation and elastic scattering. All events shown are for anti-kt reconstructed jets with $R = 0.2$ and $R_{med} = 5 \text{ fm}$.

FIG. 10: Variation of the coupling constant $\alpha_s$, elastic only (left) and elastic + rad (right), for jets in a medium at $T = 250 \text{ MeV}$ reconstructed with anti-kt $R = 0.2$. 
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[1] G. Aad et al. (Atlas), Phys. Rev. Lett., 105, 252303 (2010).
[2] S. Chatrchyan et al. (CMS Collaboration), Phys. Rev., C84, 024906 (2011).
[3] G.-Y. Qin and B. Müller, Phys. Rev. Lett., 106, 162302 (2011).
[4] C. Young, B. Schenke, S. Jeon, and C. Gale, (2011), arXiv:1103.5769 [nucl-th].
[5] C. E. Coleman-Smith, S. A. Bass, and D. K. Srivastava, (2011), arXiv:1101.4895 [hep-ph].
[6] Y. He, I. Vitev, and B.-W. Zhang, (2011), arXiv:1105.2566 [hep-ph].
[7] T. Renk, (2012), arXiv:1202.4579 [hep-ph].
[8] Geiger, Klaus and Müller, Berndt, Nucl. Phys., B369, 600 (1992).
[9] S. A. Bass, B. Müller, and D. K. Srivastava, Phys. Lett., B551, 277 (2003).
[10] P. B. Arnold and W. Xiao, Phys. Rev., D78, 125008 (2008).
[11] G. R. Shin, S. A. Bass, and B. Müller, J. Phys., G37, 105112 (2010).
[12] T. Sjöstrand, S. Mrenna, and P. Z. Skands, JHEP, 0605, 026 (2006).
[13] T. Sjöstrand, “Pythia 8 status report,” (2008).
[14] M. Cacciari and G. P. Salam, Phys. Lett., B641, 57 (2006).
[15] L. D. Landau and I. J. Pomeranchuk, Dokl. Akad. Nauk. SSSR, 92 (1953).
[16] A. B. Migdal, Phys. Rev., 103, 1811 (1956).
[17] K. Zapp, J. Stachel, and U. A. Wiedemann, Phys. Rev. Lett., 103, 152302 (2009).
[18] R. Baier, Y. L. Dokshitzer, S. Peigne, and D. Schiff, Phys. Lett., B345, 277 (1995); R. Baier, Y. L. Dokshitzer, A. H. Mueller, S. Peigne, and D. Schiff, Nucl. Phys., B478, 577 (1996); B483, 291 (1997).
[19] B. G. Zakharov, JETP Lett., 63, 952 (1996); 65, 615 (1997).
[20] M. Cacciari, G. P. Salam, and G. Soyez, JHEP, 04, 063 (2008), 0802.1189.
[21] Y. L. Dokshitzer, V. A. Khoze, A. H. Mueller, and S. I. Troian, Basics of perturbative QCD (Editions Frontieres, 1991).
FIG. 11: Variation of the jet radial profile at $T = 250$ MeV (left) and $T = 350$ MeV (right). Leading jet profiles are shown as solid lines and sub-leading jets are dashed, elastic only jets are red and radiative + elastic jets are orange. Note the strong softening of the sub-leading jet profiles and the clear separation of the elastic and radiative cases.

FIG. 12: Variation of the jet radial profile at $T = 350$ MeV. Leading jet profiles are shown as solid lines and sub-leading jets are dashed, elastic only jets are shown on the left and radiative + elastic jets are on the right. Increasing $\alpha$ strongly modifies the sub-leading jet profiles, note that the elastic (left) and radiative (right) sub-leading profiles take different shapes as $\alpha \to 0.6$. 
FIG. 13: The $z$ distribution for partonic jets at $T = 350$ MeV for jets reconstructed at $R = 0.2$ for elastic jets (left) and radiative+elastic (right). Leading jets are shown as open triangles and sub-leading jets are shown as crosses. The vacuum distributions are shown as red solid lines and the evolved distributions as blue dashed lines.

FIG. 14: The $z$ distribution for partonic jets at $T = 350$ MeV for jets reconstructed at $R = 0.4$ for elastic jets (left) and radiative+elastic jets (right). Leading jets are shown as open triangles and sub-leading jets are shown as crosses. The vacuum distributions are shown as red solid lines and the evolved distributions as blue dashed lines.
FIG. 15: The $j_t$ distribution for partonic jets at $T = 350$ MeV for jets at $R = 0.2$, elastic only jets are shown on the left with elastic+radiative jets on the right. Leading jets are shown as open triangles and sub-leading jets are shown as crosses. The vacuum distributions are shown as red solid lines and the evolved distributions as blue dashed lines.