Ultrafast control of fractional orbital angular momentum of microlaser emissions

Zhifeng Zhang, Haoqi Zhao, Danilo Gomes Pires, Xingdu Qiao, Zihe Gao, Josep M. Jornet, Stefano Longhi, Natalia M. Litchinitser and Liang Feng

Abstract

On-chip integrated laser sources of structured light carrying fractional orbital angular momentum (FOAM) are highly desirable for the forefront development of optical communication and quantum information-processing technologies. While integrated vortex beam generators have been previously demonstrated in different optical settings, ultrafast control and sweep of FOAM light with low-power control, suitable for high-speed optical communication and computing, remains challenging. Here we demonstrate fast control of the FOAM from a vortex semiconductor microlaser based on fast transient mixing of integer laser vorticities induced by a control pulse. A continuous FOAM sweep between charge 0 and charge +2 is demonstrated in a 100 ps time window, with the ultimate speed limit being established by the carrier recombination time in the gain medium. Our results provide a new route to generating vortex microlasers carrying FOAM that are switchable at GHz frequencies by an ultrafast control pulse.

Introduction

The vectorial nature of light empowers full control over topological features with spatially phase-variant fields, revealing vortex beams carrying orbital angular momentum (OAM) and spin angular momentum (SAM) in addition to the well-known linear momentum. Owing to the intriguing properties of optical vortices, OAM beams have found numerous applications in particle guiding and trapping, optical communication, quantum computation, holography and high-precision imaging, and novel light–matter interactions with topological materials. Only quite recently have optical beams carrying a fractional orbital angular momentum (FOAM) attracted considerable attention for their unusual properties and potential applications. FOAM beams display subtle topological features, and their propagation manifests some unusual mathematics of transfinite numbers.

The total angular momentum associated with electromagnetic (EM) fields in a homogeneous medium, such as free space, is

\[ \mathbf{J} = \int d^3 \mathbf{r} \varepsilon_0 \mathbf{r} \times (\mathbf{E} \times \mathbf{B}) \]

where \( r \) is the position, \( \varepsilon_0 \) is the dielectric permittivity of free space, and \( \mathbf{E} \) and \( \mathbf{B} \) are the electric field and magnetic flux density of the EM wave, respectively. In the paraxial limit, the phase variation and polarization state of an optical beam are uncoupled, featuring two independent types of angular momenta: OAM (\( \mathbf{L} \)) and SAM (\( \mathbf{S} \)).

\[ \mathbf{J} = \varepsilon_0 \sum_i \int d^3 \mathbf{r} E_i^\perp \times (\mathbf{r} \times \mathbf{A})^\perp + h.c. \]

\[ + \varepsilon_0 \int d^3 \mathbf{r} E^\perp \times A^\perp + h.c. = \mathbf{L} + \mathbf{S} \]

where \( \mathbf{E}^\perp \) and \( \mathbf{A}^\perp \) are the transverse components of the electric field and vector potential, respectively, and \( i \) denotes the order of the mode. Note that any EM wave or field can be described as a superposition on...
the eigenbasis of the Laguerre–Gaussian modes:

\[ \vec{E} = \sum_l P_{l,s} \vec{E}_{l,s} \]  

and  

\[ \vec{A} = \sum_l P_{l,s} \vec{A}_{l,s} \]

each of which carries the OAM of \( \ell \hbar \) depending on their azimuthal order \( l \) (\( l \) must be an integer) regardless of their spin state of \( \pm s \) (\( s = \pm 1 \)), where \( P_{l,s} \) represents the amplitude of each eigenmode. Due to mode orthogonality, the interference between different eigenmodes does not yield any additional OAM or spin, other than the intrinsic angular momentum associated with each mode. In this scenario, it is easily derived that the mean OAM and spin of an optical beam are (see “Materials and methods”):

\[ \langle L_z \rangle = \frac{\sum_l |P_{l,s}|^2 \hbar l}{\sum_l |P_{l,s}|^2} \quad \text{and} \quad \langle S_z \rangle = \frac{\sum_l |P_{l,s}|^2 \hbar s}{\sum_l |P_{l,s}|^2} \]

suggesting that the average OAM charge per photon in a complex field can take fractional numbers, i.e. FOAM. The ability of FOAM beams to carry any value between two (or multiple) integer numbers of quanta, as a result of superposition of two (or multiple) spatially variant fields of different vorticities, makes them especially useful in certain types of optical communications. For example, this feature leads to an increase in the modulation of the optical gain in a semiconductor (microlasers), owing to the relatively fast electron–carrier recombination dynamics of the gain medium, a series of high-speed modulation schemes can be applied to manoeuvre the in-plane chiral modes, which further facilitates ultrafast tunability and reconfigurability in OAM. To demonstrate FOAM control on the picosecond time scale, we consider our recently developed tuneable vortex microlaser consisting of a microring resonator and an external coupling loop with two control arms, all made of 200-nm-thick InGaAsP multiple quantum wells and embedded in a Si_{3}N_{4} substrate (Fig. 1). The microring resonator supports two chiral modes: counterclockwise (\( \odot \)) and clockwise (\( \odot \)) whispering gallery modes (WGMs) that are indirectly coupled by the external loop. The in-plane chiral modes are extracted and converted to OAM emissions by an angular grating with \( M \) equidistant scatters placed at the inner sidewall of the microring. In this work, we designed a microring resonator with a diameter of 7 \( \mu \)m and a width of 0.6 \( \mu \)m (see the inset in Fig. 2a). For the wavelength of approximately 1500 nm, the resonant order of the WGMs is \( N = 34 \), which, along with the diffraction order of the angular grating of \( M = 35 \), yields a total angular momentum of \( J = \pm 1 \) for emissions extracted from the \( \odot \) and \( \odot \) modes (see “Materials and methods”). The polarization state of extracted fields is, in general, a superposition of two transverse SAMs (i.e. left-handed (\( s = 1 \)) and right-handed (\( s = -1 \)) circular polarizations), with their amplitudes geometrically dependent on the dimensions of the microring. Therefore, the microlaser emissions contain 4 components...
corresponding to the 4 SAM–OAM combinations, described as:

\[ I_{\text{out}} = I_{L,-2} + I_{L,0} + I_{R,0} + I_{R,+2} \]

\[ \times p_{C} \sigma^2 + p_{C} (1 - \sigma^2) + p_{C} (1 - \sigma^2) + p_{C} \sigma^2 \]

where \( I_{\text{out}} \) is the total intensity of the microlaser emissions, which is the sum of the intensities of 4 different spin–OAM components, with \( L/R \) indicating left/right-handed circular polarization and \(-2, 0, +2\) denoting the associated OAM charge. The four spin–OAM components correspond to the out-couplings of the four combinations between the \( \varpi/\rho \) mode and in-plane transverse spins, where \( p_{\varpi}/p_{\rho} \) denotes the power associated with the \( \varpi/\rho \) mode inside the cavity, respectively, and \( \sigma \) is the absolute value of the transverse SAM charge to describe the purity of the transverse spin. Equation (4) captures the central idea of this work—by exciting and reconfiguring the weighting of different OAM components, we demonstrate a precise, continuous FOAM sweep between charge 0 and charge +2 within 100 ps. The associated FOAM charge is calculated by integrating the OAM flux across the entire vector beam (see the spatially varying polarization state shown in the inset of Fig. 1)\(^{34,35}\), according to Eq. (3), given no spin–orbit coupling at the paraxial limit after the beam is emitted from the microlaser.
The WGM microlaser emission is controlled by exploiting indirect non-Hermitian mode coupling\(^{36-39}\) via suitable external loops\(^{31}\); see Fig. 1. The effective mode coupling can be turned from completely symmetric (Hermitian) to unidirectional (exceptional point), depending on the gain–loss contrast between the two control arms. This enables active tuning of the weighting between the two chiral modes (which is equivalent to the power ratio between \(p_\Omega\) and \(p_{\text{OC}}\)) (see “Materials and methods”). To achieve ultrafast control, we apply two synchronized femtosecond pulses from the same femtosecond laser (~140 fs) to pump the entire structure: a main pump pulse above the lasing threshold at time \(T_1\) to enable lasing oscillation in the microring and a control pulse below the lasing threshold at time \(T_2\) to selectively excite gain carriers in one of the two arms. In addition to control of the peak gain via the pump power, here the transient carrier dynamics with a carrier lifetime typically of hundreds of picoseconds are the key to ultrafast control. As the excited carriers relax with time after pulse pumping, the associated gain coefficient also decays, as does the gain–loss contrast between the two control arms. Consequently, the non-Hermitian-controlled indirect coupling dynamically varies as a function of time, from unidirectional to symmetric. Hence, temporal overlap of the laser action in the microring and the time-varying optical gain in the control arm, precisely controlled by the time delay between the two femtosecond pump pulses, facilitates ultrafast control of the weighting between the two chiral modes in the microring and thus the weighting between different mode-converted OAM components in Eq. (4), yielding dynamic tuning of the FOAM of microlaser emissions with a picosecond resolution (Fig. 1).

In experiments, the emitted vortex beam was collected by a ×20 microscope objective and guided through a charge-coupled device (CCD) camera (Fig. 2a). The spectrum of the microlaser emissions confirms single-frequency laser action at the wavelength of 1494.6 nm with a sideband suppression ratio of >24 dB (Fig. 2b). To experimentally validate the transient carrier dynamics, we projected the control pulse to spatially overlap with the main pulse on the microring. The power of microlaser emissions, contributed by both pulses, was continuously captured as a function of the time delay between the two ultrafast pulses, i.e. \(T_1 - T_2\) (Fig. 2c). If the two pulses are temporally far apart (i.e. \([T_1 - T_2] \gg 0\)), then the emitted power is equivalent to the summation of the two individual laser actions/spontaneous emissions, as there is no temporal overlap of gain carriers excited by the two pulses. When the two pulses are close in time (not overlapped), the two pulses collectively boost the emitted power: for example, if the control pulse arrives first and a substantial amount of its excited carriers survive until the arrival of the main pulse, then the carriers excited by the two pulses augment each other, leading to significant enhancement in the power of the laser emissions. Nevertheless, the strongest enhancement does not occur at zero time delay (i.e. \(T_1 - T_2 = 0\)). In contrast, the first arrival of a strong pumping pulse depletes the carriers in the ground state, causing reduced absorption of the control pulse and thus leading to a sudden drop in the output power of the microlaser emissions\(^{40,41}\). The data afterwards exhibit a gain carrier lifetime of \(\tau = 263.15 \pm 1.41\) ps in the InGaAsP multiple quantum wells, demonstrating the potential for ultrafast dynamic control (see Supplementary Information).

As discussed above, a precise, continuous FOAM sweep can be realized by exciting and reconfiguring the weighting of different OAM components. Ultrafast temporal control of the weighting between the two chiral modes and thus of the ratio between their associated powers (\(p_{\text{OC}}/p_{\text{OC}}\)), which is the key dynamic parameter to reconfigure the fraction of each spin–OAM component in the emitted vector beam [see Eq. (4)], is achieved by tuning the temporal delay between the main pulse incident on the microring and the control pulse in the left control arm. In particular, the modulation of the carriers, facilitated by the precisely controlled temporal delay of the pulses in both the microring and the left control arm, enables ultrafast control of the fractional OAM charge. Note that \(\sigma\) is geometrically defined and fixed after the sample is fabricated. The power associated with all four spin–OAM components in Eq. (4) can be evaluated according to their spatial distributions and polarization states. For instance, the \(|R, 0\rangle\) and \(|L, 0\rangle\) states are located at the centre, as marked in the inset of Fig. 3a. By selectively capturing the power of each polarization state, the temporal response of lasing chirality, defined as \(\langle p_{\text{OC}} - p_{\text{OC}}\rangle/(p_{\text{OC}} + p_{\text{OC}})\), is depicted in Fig. 3a (see Supplementary Information). Similarly, the temporally varying power associated with \(|R, +2\rangle\) and \(|L, -2\rangle\) can be measured: as the time delay approaches zero, the chirality reaches 1 (i.e. \(p_{\text{OC}} \gg p_{\text{OC}}\)), leading to the maximum weighting of \(|R, +2\rangle\) and zero \(|L, -2\rangle\) (Fig. 3d, e). Altogether, by counting the power weighted average of all 4 integer OAM components, we conducted dynamic sweeping of the FOAM charge of the vector beam with a picosecond resolution, where the fractional charge could rapidly vary from 0.18 to 1.57 within 100 ps (Fig. 3b). The upper bound of the tuning range can be expanded if the cross-spin components are filtered. By selecting only the right-handed polarized components (\(|R, +2\rangle\) and \(|R, 0\rangle\)), the FOAM charge varies in the range from 1.68 to 2 (Fig. 3c). Figure 3d, e show the histograms of decomposed integer OAM orders at five different time delays,
with and without filtering the cross-spin components, respectively. Note that, because the $|R, +2\rangle$ and $|L, 0\rangle$ states are both locked with the same $\mathcal{O}$ mode, OAM charge 0 cannot vanish without filtering out the cross-spin components (Fig. 3d). The desired polarization selection further promotes the upper bound of the FOAM tuning to pure OAM charge 2, despite the generalized condition of a nonunitary transverse spin in our design (Fig. 3e). It is also worth noting that, due to the finite duration of the laser output pulse (<20 ps), the measured results correspond to the temporal average of the FOAM throughout the duration of the output pulse.

The phase singularity, associated with zero intensity at the singularity point, is a unique topological feature of the vortex beam. The ultrafast control enables novel space–time photonic transitions with dynamically evolving beam characteristics, as revealed by the splitting and merging of singularity points in the vector beam on the picosecond scale (Figs. 4 and 5). In the case without polarization selection (Fig. 4), all 4 spin–OAM components spatially superpose: $|R, +2\rangle$ and $|L, -2\rangle$ spatially overlap, but their opposite azimuthal phase variations cancel each other, while the two OAM charge 0 components ($|R, 0\rangle$ and $|L, 0\rangle$) carry planar phase fronts with a bright spot at the centre of the vortex beam at $|T_1 - T_2| \geq 80$ ps. Therefore, the microlaser emissions are nonchiral, and the simulated phase map does not indicate any pronounced phase singularity, consistent with the continuous interference fringes experimentally observed via the off-centre self-interference of the emitted vector beam. Note that the beam is in general elliptically polarized when including all four spin–OAM components. The phase of the beam in Fig. 4a is defined as $\phi = \arg(E^T S)$, where $E$ is the electric field vector and $S$ is the unit elliptical polarization vector: $S = \frac{1}{\sqrt{|E_x|^2 + |E_y|^2}} \begin{bmatrix} |E_x| e^{-i \alpha} \\ |E_y| e^{i \alpha} \end{bmatrix}$, where $E_x$ and $E_y$ are the x and y components of the electric field and $\alpha$ is the phase delay between them. As $p_0$ prevails when the time delay between the two pulses approaches zero, $|R, +2\rangle$ and $|L, 0\rangle$ become dominant, leading to a dynamically increased FOAM charge. In a very short duration, two charge +1 singularity points emerge from the bright doughnut area and move towards the centre, as evidently shown in the measured interferograms: two forks are formed due to phase
**Fig. 4** Temporal evolution of the FOAM laser emissions without filtering out the cross-spin components.  

- **a** Simulated phase distribution $\phi$ of the elliptically polarized FOAMs at 5 different time delays between the pump and control pulses, carrying a fractional charge of $l = 0.18, 0.55, 1.57, 0.82, \text{ and } 0.23$. Two singularity points associated with the FOAM vortex field emerge from the edges and move towards the centre as the delay time approaches zero.  
- **b** Measured off-centre self-interferences of FOAM vortex fields at the five time delays. The images are cropped to show the fine details (see Supplementary Information). As the time delay approaches zero, forks arise from the two singularity points of the FOAM field and move towards the centre. Forks are marked with white dashed lines for better visibility.  
- **c** Measured intensity maps of the FOAM field, featuring dark holes around a bright centre that arises from OAM charge 0 components (i.e. $|R,0\rangle$ and $|L,0\rangle$). The two dark holes become less visible when the delay time approaches zero, as they become spatially overlapped with only the $|L,0\rangle$ component.

**Fig. 5** Temporal evolution of the FOAM laser emissions after filtering out the cross-spin components.  

- **a** Simulated phase distribution $\phi$ of the right-handed circularly polarized FOAMs at 5 different time delays between the pump and control pulses, carrying a fractional charge of $l = 1.68, 1.8, 2, 1.86, \text{ and } 1.71$. Two charge $+1$ singularity points associated with the FOAM vortex field move towards the centre and finally merge at zero time delay.  
- **b** Measured off-centre self-interferences of FOAM vortex fields at the five time delays. The images are cropped to show the fine details (see Supplementary Information). Two separated charge $+1$ forks merge at zero time delay, where a single fringe splits into three, indicating an OAM charge of $+2$. Forks are marked with white dashed lines for better visibility.  
- **c** Measured intensity maps of the FOAM field, where the bright centre arises from the same-spin OAM charge 0 component (i.e. $|R,0\rangle$). As the two singularity points merge at the centre at zero time delay, the bright centre (i.e. $|R,0\rangle$) vanishes, featuring a pure OAM charge of $+2$ (i.e. $|R,+2\rangle$).
However, our set-up can be easily modified to observe these phenomena. The two charge +1 singularity points cannot touch because of the existence of \(|L, 0\rangle\) arising from the geometrically defined \(\sigma\) associated with the nonunitary transverse spin. However, with successful filtering out of the cross-spin components \(L\) (Fig. 5), only \(|R, +2\rangle\) survives at \(T_1 - T_2 = 0\), so the two charge 1 singularity points merge to form a charge +2 singularity, manifested by a perfect doughnut with a 4\(\pi\) phase variation in the azimuthal direction. Since only the right-handed circularly polarized components remain, the phase of the beam in Fig. 5a is defined as \(\phi = \arg(E^2 R)\), where \(E\) is the electric field vector and \(R\) is the unit vector of the right-handed circular polarization, 

\[
R = \frac{1}{\sqrt{2}} \left[ \frac{1}{e^{-i\phi/2}} \right].
\]

In the off-centre self-interference of the emitted beam, the fork-like fringe splits from 1 to 3, confirming a topological charge of +2. When the two pump pulses do not temporally overlap (i.e. \(T_1 - T_2 \neq 0\)), \(|R, +2\rangle\) and \(|R, 0\rangle\) coexist, also leading to a dynamically tuned FOAM charge with two charge +1 singularity points. In this case, the dynamic FOAM tuning ranges from 1.68 to 2, where the lower bound is mainly determined by the parameter \(\sigma\) given comparable \(p_C\) and \(p_D\) at \(|T_1 - T_2| \approx 80\) ps.

**Discussion**

We have experimentally demonstrated ultrafast FOAM modulation in a continuously tuneable vortex microlaser, harnessing the fast transient carrier dynamics of the semiconductor optical gain in conjunction with non-Hermitian-controlled spin–orbital interactions of light. Notably, the switching speed of the FOAM vortex emission is in principle limited by the semiconductor optical response, with the potential to achieve sub-ps switching on other material platforms, such as perovskites. The demonstrated FOAM tuning ranges from charge 0 to +2. However, our set-up can be easily modified to temporally coordinate ultrafast pumping on both control arms so that the vortex microlaser can in principle emit any FOAM state from charge \(-2\) to \(+2\), dynamically controlled with a picosecond resolution. Our scheme with ultrafast control of continuously tuneable FOAM, compatible with other modulation schemes in polarization, amplitude, frequency, etc., could be of potential relevance for the next generation of ultrahigh-speed optical communication systems, offering a feasible route to further enhancing the communication bandwidth based on multilevel OAM keying in coherent optical communication. Additionally, it could be exploited to reveal novel topological space–time features associated with pulsed vector beams.

**Materials and methods**

**Angular momentum associated with an EM wave**

In the derivation, we apply the Coulomb gauge: \(\nabla \cdot \vec{A} = 0\) and \(\phi = 0\) under the source-free condition. The vector potential of light radiated by our device can be expressed as:

\[
\vec{A} = \sum_{s,l} -l^{-1} \frac{PM}{2\pi} \frac{k^2}{l^2} \Phi(\rho, z) I_{l-1} (-k \frac{\rho}{l}) \exp[j(l-1)\phi] \vec{e}_s
\]

\[
= \sum_{s,l} P_{s,l} \vec{A}_{s,l.}
\]

where \(P\) is the radiation intensity of each scatter, \(M\) is the number of scatterers, \(s\) is the radius of the ring resonator,

\[
P_{s,l} = \sqrt{\int_{\Omega} \frac{[e^{-l^{-1} PM \Phi(\rho, z) I_{l-1} (-k \frac{\rho}{l}) \exp[j(l-1)\phi] \vec{e}_s]^2]}{\rho^{2\pi}} dV}
\]

is the amplitude of each mode with normalization condition:

\[
\int_{\Omega} \vec{A}_{s,l.}^2 dV = 1
\]

\(k\) is the wavevector, \(\omega\) is the angular frequency, \(\Phi(\rho, z) = \exp\left[jk \left(z + \frac{\rho^2}{2l^2}\right)\right]\) is a phase factor, \(s\) represents spin as aforementioned, and \(\vec{e}_{-1} = (\vec{e}_x - i \vec{e}_y) / \sqrt{2}\) and \(\vec{e}_{+1} = (\vec{e}_x + i \vec{e}_y) / \sqrt{2}\) are the unit vectors of right and left circular polarization, respectively. Correspondingly, the electric field can be expressed as:

\[
\vec{E} = \sum_{s,l} -l^{-1} \frac{PM}{2\pi} \Phi(\rho, z) I_{l-1} (-k \frac{\rho}{l}) \exp[j(l-1)\phi] \vec{e}_s
\]

\[
= \sum_{s,l} P_{s,l} \vec{E}_{s,l.}
\]

To calculate the mean value of OAM and spin, note that:

\[
\int_{\Omega} \Phi(\rho, z) I_{l-1} (-k \frac{\rho}{l}) \exp[j(l-1)\phi] \vec{e}_s dV = 2\pi \delta_{l,2} \delta_{s,0}
\]

\[
\int_{\Omega} \Phi(\rho, z) I_{l-1} (-k \frac{\rho}{l}) \exp[j(l-1)\phi] \vec{e}_s \times \vec{e}_z dV = 2\pi js_{l,2} \delta_{s,0} \vec{e}_z
\]

With the OAM and spin associated with each individual mode:

\[
\left( \int_{\Omega} \Phi(\rho, z) I_{l-1} (-k \frac{\rho}{l}) \exp[j(l-1)\phi] \vec{e}_s dV \right)_z = \hbar I_{l,1}
\]

\[
\left( \int_{\Omega} \Phi(\rho, z) I_{l-1} (-k \frac{\rho}{l}) \exp[j(l-1)\phi] \vec{e}_s \times \vec{e}_z dV \right)_z = \hbar s_{l,1}
\]

we find the mean OAM and mean spin of the field as described in Eq. (3).
Ultrafast non-Hermitian chiral control

In the case of pumping the main microring and the left control arm as implemented in our experiment (Fig. 1), the ultrafast chiral response of our tuneable vortex microlaser can be described by the following coupled mode equations when \( T_1 - T_2 \geq 0 \) by assuming a fast response of carriers:

\[
\frac{dE_\Omega}{dt} = i\omega E_\Omega + (\kappa_0 + \kappa_0 e^{-\tau}) e^{(-i\omega t + i\kappa_0 t)} E_\Omega,
\]

\[
\frac{dE_\Theta}{dt} = i\omega E_\Theta + (\kappa_0 + \kappa_0 e^{-\tau}) E_\Theta,
\]

where \( E_\Omega/E_\Theta \) denotes the electric field amplitude of the \( \Omega/\Theta \) mode, respectively; \( \kappa \) is the coupling between \( \Omega \) and \( \Theta \) modes without gain or loss; \( \kappa_0 \) corresponds to the coupling arising from the nonlinear effects and fabrication imperfections; \( -\gamma \) is the single pass attenuation through the control waveguide; \( \gamma_L \) indicates the single pass amplification through the control waveguide at the time of pulse incidence; and \( \tau \) is the lifetime of gain carriers in the control waveguide. The power ratio between the two chiral modes circulating in the microring can be roughly estimated from the steady-state linear supermode analysis and reads as:

\[
P_\Omega/P_\Theta = \left( \frac{E_\Omega}{E_\Theta} \right)^2 = \frac{\kappa_0 + \kappa_0 e^{-\tau}}{\kappa_0 + \kappa_0 e^{-\tau}}.
\]

Note that the carrier dynamics are assumed to have an instantaneous and linear impact on the chiral ratio because the pump pulse duration is several orders of magnitude shorter than the carrier lifetime, while the lasing pulse duration is shorter than \( \tau \). Numerical analysis of laser pulse dynamics, based on semiconductor rate equations\(^46\) with spontaneous emission noise, shows that the ratio of pulse energies between the two chiral modes circulating in the ring is well described by the above equation.

Design of transverse spin

The transverse spin, in which the electric field rotates around the axis perpendicular to the propagation direction of light\(^47,48\), is designed by inspecting the value of \( \frac{|E^L|}{|E^R|} \) through full-wave numerical simulations, where \( E \) denotes the electric field vector and \( R \) denotes the unit vector of right-hand circular polarization. With the geometric configuration of the microring, 200 nm in height and 600 nm in width, \( \frac{|E^L|}{|E^R|} \) is 0.9, which is equivalent to \( \sigma = 0.9 \), indicating the purity of the transverse spin.

Extraction of OAM

An angular grating of order \( M \) is placed at the inner sidewall of the microring to extract the \( N \)th order WGMs. The local phase at the \( q \)th scatter position can be written as \( \phi_{q,local} = 2\pi Cq(N - M)/M \), where \( q \in \{0, M - 1\} \) and \( C = \pm 1 \) for the \( \Omega \) and \( \Theta \) modes. Due to the nonunitary transverse spin, the extracted global phases experience opposite coordinate rotation and can be expressed as \( \phi_{global,q} = 2\pi C^q(N - M) - q)/M \) for the left-handed spin (\( s = 1 \)) component and \( \phi_{global,q} = 2\pi C^q(N - M) - q)/M \) for the right-handed spin (\( s = -1 \)) component. Therefore, the linearly varying phase distribution creates an emission with two integer OAM modes with topological charges of \( C(N - M - 1) \) and \( C(N - M + 1) \) with orthogonal spin states and a total angular momentum \( |J| = |N - M| \).

Sample fabrication and characterization

The tuneable vortex microlaser was fabricated using electron-beam lithography, inductively coupled plasma etching (ICP), plasma-enhanced chemical vapour deposition (PECVD), and substrate transfer techniques. Hydrogen silsesquioxane (HSQ) in methyl isobutyl ketone (MIBK) solution was used for patterning. The concentration ratio of HSQ (FOX15) to MIBK was adjusted such that an adequately thick layer of resist was formed for etching after exposure and development. The patterned wafer was then immersed and slightly stirred in tetrachloroethylene solution (MFC26) and rinsed in deionized water. The chip was subsequently processed by ICP dry etching with BCl3 and Ar, followed by removal of HSQ resist using buffered oxide etchant. Next, a Si$_3$N$_4$ cladding was deposited by PECVD. The wafer was then bonded to a glass slide, which functioned as a base. Finally, the InP substrate was removed by wet etching with a mixture of HCl and H$_3$PO$_4$.

The fabricated tuneable vortex microlaser was pumped on the front side by a femtosecond pulsed laser with an 80 MHz repetition rate and a 140 fs pulse duration at a wavelength of 800 nm. The pump power was controlled with a variable neutral density filter, monitored by a power meter. The pump pulse was reflected by a 50:50 beam splitter and focussed onto the microring cavity using a Mitutoyo ×20 near-infrared long-working-distance objective (NA = 0.4). The additional control pump pulse was tuned with a half waveplate together with a polarization beam splitter and projected onto the control arms through a Mitutoyo ×10 long-working-distance objective (NA = 0.28) from the backside (through the SiN substrate). The delay time between these two pulses was controlled by a motorized linear translation stage. The laser emission from the front side was collected by the aforementioned ×20 microscope objective, guided through a quarter waveplate and a linear polarizer for the desired polarization selection, and then recorded on a CCD camera. A Michelson interferometer was built to measure the off-centre self-interference of the beam to analyse the beam characteristics.
We acknowledge the support from the National Science Foundation (NSF) (EECS-1932803, OMA-1936276, ECCS-1842612, DMR-1809518, and CNS-2011441), U.S. Army Research Office (ARO) (W911NF-19-1-0249 and W911NF-18-1-0348), and Office of Naval Research MURI (N00014-20-1-2558). This research was partially supported by the NSF through the University of Pennsylvania Materials Research Science and Engineering Center (MRSEC) (DMR-1720530). This work was carried out in part at the Singh Center for Nanotechnology, which is supported by the NSF National Nanotechnology Coordinated Infrastructure Program under grant NNI3-1542153.

Author details
1Department of Electrical and Systems Engineering, University of Pennsylvania, Philadelphia, PA 19104, USA. 2Department of Electrical and Computer Engineering, Duke University, Durham, NC 27708, USA. 3Department of Materials Science and Engineering, University of Pennsylvania, Philadelphia, PA 19104, USA. 4Department of Electrical and Computer Engineering, Northeastern University, Boston, MA 02115, USA. 5Dipartimento di Fisica, Politecnico di Milano and Istituto di Fotonica e Nanotecnologie del Consiglio Nazionale delle Ricerche, Piazza L. da Vinci 32, I-20133 Milano, Italy. 6Instituto de Fisica Interdisciplinar y Sistemas Complejos IFISC (CSIC-UIB), Palma de Mallorca, Spain.

Author contributions
Z.Z. and L.F. conceived the project and conducted the design. Z.Z., H.Z., D.G.P., Z.G., N.M.I., S.L., and L.F. constructed the theoretical model and numerical simulations. X.Q. fabricated the samples. Z.Z. and H.Z. performed the measurements: Z.Z., H.Z., D.G.P., L.F., N.M.I., S.L., and J.M.I. carried out data analyses. All authors contributed to manuscript preparation and discussion.

Conflict of interest
The authors declare that they have no conflict of interest.

Supplementary information is available for this paper at https://doi.org/10.1038/s41377-020-00415-3.

Received: 12 August 2020 Revised: 28 September 2020 Accepted: 29 September 2020 Published online: 21 October 2020

References
1. Padgett, M., Courtial, J. & Allen, L. Light’s orbital angular momentum. Phys. Today 57, 35–40 (2004).
2. Shen, Y. J. et al. Optical vortices 30 years on: OAM manipulation from topological charge to multiple singularities. Light Sci. Appl. 8, 90 (2019).
3. Du, L. P. et al. Deep-subwavelength features of photonic skyrmions in a confined electromagnetic field with orbital angular momentum. Nat. Phys. 15, 462–464 (2019).
4. He, H. et al. Direct observation of transfer of angular momentum to absorptive particles from a laser beam with a phase singularity. Phys. Rev. Lett. 75, 826–829 (1995).
5. Wang, J. et al. Terabit free-space data transmission employing orbital angular momentum multiplexing. Nat. Photonics 6, 488–496 (2012).
6. Bozovic, N. et al. Terabit-scale orbital angular momentum mode division multiplexing in fibers. Science 340, 1545–1548 (2013).
7. Torner, L., Torres, J. P. & Carasco, S. Digital spiral imaging. Opt. Express 13, 873–881 (2005).
8. Ji, Z. R. et al. Photocurrent detection of the orbital angular momentum of light. Science 368, 763–767 (2020).
9. Gou, G. Fractional vortex Hilbert’s hotel. Optica 3, 222–225 (2016).
10. Barnett, S. M. et al. On the natures of spin and orbital parts of optical angular momentum. J. Opt. 18, 046004 (2016).
11. Molina-Terriza, G., Torres, J. P. & Torner, L. Management of the angular momentum of light: preparation of photons in multidimensional vector states of angular momentum. Phys. Rev. Lett. 88, 013601 (2001).
12. Liu, Y. et al. Multi-dimensional OAM equivalent constellation using coherently coupled orbital angular momentum (OAM) modes in optical communication. Opt. Express 26, 30969–30977 (2018).
13. Mauer, C. et al. What spatial light modulators can do for optical microscopy. Laser Photonics Rev. 5, 81–110 (2011).
14. Pan, Y. et al. Arbitrarily tunable orbital angular momentum of photons. Sci. Rep. 6, 29212 (2016).
15. Berry, M. V. Optical vortices evolving from helicoidal integer and fractional phase steps. J. Opt. A Pure Appl. Opt. 6, 259–268 (2004).
16. Leach, J., Yao, E. & Padgett, M. J. Observation of the vortex structure of a non-integer vortex beam. J. Phys. 6, 71 (2004).
17. Devlin, R. C. et al. Arbitrary spin-to-orbital angular momentum conversion of light. Science 353, 464–467 (2016).
18. Zhang, J. et al. An InP-based vortex beam emitter with monolithically integrated laser. Nat. Commun. 9, 2652 (2018).
19. Zamboni, N. C. et al. Optically controlling the emission chirality of microlasers. Nat. Photonics 13, 283–288 (2019).
20. Li, G. X., Zhang, S. & Zentgraf, T. Nonlinear photonic metasurfaces. Nat. Rev. Mater. 2, 17010 (2017).
21. Xu, Y. et al. Reconfiguring structured light beams using nonlinear metasurfaces. Opt. Express 26, 30930–30943 (2018).
22. Zhang, Z. F. et al. Tunable topological charge vortex microlaser. Science 368, 760–763 (2020).
23. Ca, X. L. et al. Integrated compact optical vortex beam emitters. Science 338, 363–366 (2012).
24. Jiang, X. F. et al. Whispering-gallery microcavities with unidirectional laser emission. Laser Photonics Rev. 10, 40–61 (2016).
25. Allen, L. et al. Orbital angular momentum of light and the transformation of Laguere-Gaussian laser modes. Phys. Rev. A 45, 8185–8189 (1992).
26. Longhi, S. & Fong, L. Unidirectional lasing in semiconductor microring lasers at an exceptional point [Invited]. Photonics Res. 5, 81–86 (2017).
27. Longhi, S. & Fong, L. Mitigation of dynamical instabilities in laser arrays via non-Hermitian coupling. AIP Photonics 3, 066802 (2018).
28. Longhi, S. Non-Hermitian gauged topological laser arrays. Ann. Phys. 530, 1800232 (2016).
29. Lü, S. & Della Valle, G. Robust light transport in non-Hermitian photonic lattice. Sci. Rep. 5, 13376 (2015).
30. Hall, K. L. et al. Femtosecond gain dynamics and saturation behavior in InGaAsP multiple quantum well optical amplifiers. Appl. Phys. Lett. 57, 2888–2890 (1990).
31. Sidiropoulos, T. P. H. et al. Ultrafast plasmonic nanowire lasers near the surface plasmon frequency. Nat. Phys. 10, 870–876 (2014).
32. Huang, C. et al. Ultrafast control of vortex microlasers. Science 367, 1018–1021 (2020).
33. Luo, M. D. & Wang, Z. Y. Fractional vortex ultrashort pulsed beams with modulating vortex strength. Opt. Express 27, 36259–36268 (2019).
34. Siedeh, H. B., Salany, M. M. & Mosallaei, H. Topological space-time photonics in angular-momentum-based metasurfaces. Adv. Opt. Mater. 8, 2000075 (2020).
35. Zhu, J. B. et al. Theoretical model for optical grating-based integrated optical vortex beam emitters. Opt. Lett. 38, 1343–1345 (2013).
36. Scully, M. O. & Zubairy, M. S. Quantum Optics (Cambridge University Press, Cambridge, 1999).
37. Bloch, K. et al. Spin–orbit interactions of light. Nat. Photonics 9, 896–908 (2015).
38. Shi, Z. K. et al. Spin–orbit interaction of light induced by transverse spin angular momentum engineering. Nat. Commun. 9, 926 (2018).
Supplementary Information

Ultrafast control of fractional orbital angular momentum of microlaser emissions

Zhifeng Zhang\textsuperscript{1}, Haoqi Zhao\textsuperscript{1}, Danilo Gomes Pires\textsuperscript{2}, Xingdu Qiao\textsuperscript{1}, Zihe Gao\textsuperscript{3}, Josep M. Jornet\textsuperscript{4}, Stefano Longhi\textsuperscript{5,6}, Natalia M. Litchinitser\textsuperscript{2}, and Liang Feng\textsuperscript{3,1*}

\textsuperscript{1}Department of Electrical and Systems Engineering, University of Pennsylvania, Philadelphia, PA 19104, USA

\textsuperscript{2}Department of Electrical and Computer Engineering, Duke University, Durham, NC 27708, USA

\textsuperscript{3}Department of Materials Science and Engineering, University of Pennsylvania, Philadelphia, PA 19104, USA

\textsuperscript{4}Department of Electrical and Computer Engineering, Northeastern University, Boston, MA 02115, USA

\textsuperscript{5}Dipartimento di Fisica, Politecnico di Milano and Istituto di Fotonica e Nanotecnologie del Consiglio Nazionale delle Ricerche, Piazza L. da Vinci 32, Milano I-20133, Italy

\textsuperscript{6}Instituto de Fisica Interdisciplinar y Sistemas Complejos IFISC (CSIC-UIB) - Palma de Mallorca, Spain

*Email: fenglia@seas.upenn.edu
1. **Polarization state of microlaser emissions**

   When only the microring laser is pumped, the microlaser emissions contain all 4 spin-OAM components as described in Eq. (4) and form a vector beam whose polarization state spatially varies as shown in the inset of Fig. 1 and marked in Fig. S1a. The observed bright circle corresponds to the contributions from the OAM ±2 components and the non-zero center arises from the two OAM 0 components. The spatially varying polarization nature of the beam was verified by selecting two orthogonal linear polarizations, showing two complementary 4-lobe patterns (Fig. S1b and Fig. S1c). Since the field at the center of the beam is horizontally polarized, it is visible when a linear polarizer is horizontally placed but varnishes when the polarizer is vertically aligned.

![Figure S1. a. Measured intensity pattern of the microlaser emissions with arrows indicating the polarization states. b. Measured intensity pattern of the microlaser emissions passing through a linear polarizer in the horizontal direction, showing 4 main lobes with a central line connecting the upper and lower lobes. c. Measured intensity pattern of the microlaser emissions passing through a linear polarizer in the vertical direction, showing only 4 lobes 90° rotated with respect to those in b.](image)

2. **Measurement of carrier lifetime**

   The measurement of carrier lifetime, as shown in Fig. 2c, was carried out by focusing both the main pump and control pulses onto the microring resonator and collecting the lasing emissions as a function of time delays between the two pulses. The energy of the main pump pulse is much greater than the lasing threshold, while the energy of the control pulse is lower than the lasing threshold. The polarization states of the two pulses are orthogonal, so they do not interfere and serve as two individual pumps. Note that at each time delay, the measurement corresponds to temporal integration of microlaser emissions. We also conducted two control experiments in addition to that shown in Fig. 2c: 1) both pulses’ energies are much greater than the lasing threshold and 2) both pulses’ energies are less...
than the lasing threshold but their summation is greater than the threshold when overlapped in time and space. (Fig. S2)

**Figure S2.** Measured lasing emission intensities when the microring is pumped by different combinations of energies associated with the main pump pulse and the control pulse.

When both pulses’ energies are lower than the lasing threshold, lasing only occurs within a certain range of $T_1 - T_2$. If $T_1 - T_2 > 0$, the control pulse reaches the laser cavity first and excites a number of carriers decaying in time, but some carriers remain upon the arrival of the pump pulse. In this scenario, if the sum of the carriers contributed by both pulses surpasses the lasing threshold, the laser action happens until the total carriers decay to drop below the lasing threshold.

When pump pulse has a greater energy above the lasing threshold but the control pulse is below the threshold, the laser action is always measured regardless of the time delay between the two pulses. In the region of $T_1 - T_2 < 0$, however, there are three small sub-regions exhibiting different features: (i) $< -38$ ps (the left kink), (ii) between -38 and -17 ps (peak) and (iii) between -17 and 0 ps. In region (i), the lasing triggered by the main pump pulse ends completely and its excited carriers drop below the threshold. However, the arrival of the control pulse brings the microring back to lasing since a good number of carriers remain. As a result, the captured signal, including a main lasing pulse excited by the main pump and a secondary lasing pulse triggered by the control, is enhanced but with a lower slope efficiency. In region (ii), the lasing emission is enhanced more rapidly and efficiently. Despite the decay of the carriers, the lasing action triggered by the main pump
pulse is still on-going. In this scenario, the control pulse directly contributes to the laser actions with a greater slope efficiency. The peak signal corresponds to the right time delay where the remaining carriers excited by the main pump, together with the new carriers supplied by the control, reach the maximum absorption of pulse energy corresponding to the power saturation threshold, below which the microlaser has the best slope efficiency. In this case, the carriers excited by the control pulse is converted into laser emissions with the highest efficiency, resulting in the maximum enhancement in laser emissions in time. In region (iii), a very large number of carriers are excited by the main pulse and still remain till the arrival of the control pulse. In this case, the carriers on the ground state are depleted, causing reduced absorption of the control pulse and therefore bringing the microlaser into the power saturation region with reduced energy conversion efficiency. This leads to a drop in microlaser emissions with a minimum occurring at the time when the two pulses are completely overlapped. In the region of $T_1 - T_2 > 0$, the control pulse arrives earlier and excites carriers with a lifetime $\tau$ (no lasing occurs yet). Since the control pulse is below the lasing threshold, only the spontaneous emission occurs before the arrival of the main pump pulse, where the carriers decay at the spontaneous recombination rate. The remaining carriers effectively enhance the total laser output. When $T_1 - T_2$ increases, this effective enhancement decreases in its intensity with the spontaneous recombination rate, by which data fitting was performed to retrieve the carrier lifetime: $\tau \approx 263$ ps.

When both pulses are greater than the lasing threshold with similar energy, we observed a symmetric response of output laser emissions with respect to zero time delay. Similarly, the three small regions also exist, as the aforementioned lasing mechanism still applies in this case. Note that, in the region of $T_1 - T_2$ is sufficiently large, the carriers excited by the control pulse decay to a level similar to the weak control pulse discussed above. In this case, data fitting was also performed to retrieve the carrier lifetime, which shows a similar result: $\tau \approx 249$ ps.

3. **Measurement and calculation of lasing chirality**

The chirality of the microlaser can be evaluated by $Chirality = \frac{P_{\omega}-P_{\omega}}{P_{\nu}+P_{\omega}}$. To calculate the chirality, we performed two integrations of the power in the region defined by the white dashed circle in the inset of Fig. 3a (i.e., the OAM 0 components), with (i) filtering out the
left-handed circularly polarized components and (ii) filtering out the right-handed circularly polarized components, respectively. The measured powers from these two different conditions are proportional to $p_{\leftarrow}$ and $p_{\rightarrow}$, respectively, given the same out-coupling efficiency (see Eq. (4) in the main text).

4. **Measurement and crop of off-center self-interferences patterns**

The off-center self-interference patterns were performed to validate the charge of the microlaser emissions, as shown in Fig. S3, showing 2 pairs of forks: one pair both facing up in the white box on the left half and the other pair both facing down on the right half. The opposite directions of the two pairs show their origins from the two beams in the interference. To make the results more visible and manifest detailed information, we only cropped the part in the white box and showed in Fig. 4 and Fig. 5.

![Area of interest](image)

**Figure S3.** Full image of one off-center self-interference pattern. The white box region was cropped and zoomed in to show the details in the main text. In this full image, four single charge forks (2 pairs) are observed with a pair on each side and the 2 pairs face in opposite directions.