The case for background independence*

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Abstract

The aim of this paper is to explain carefully the arguments behind the assertion that the correct quantum theory of gravity must be background independent. We begin by recounting how the debate over whether quantum gravity must be background independent is a continuation of a long-standing argument in the history of physics and philosophy over whether space and time are relational or absolute. This leads to a careful statement of what physicists mean when we speak of background independence. Given this we can characterize the precise sense in which general relativity is a background independent theory. The leading background independent approaches to quantum gravity are then discussed, including causal set models, loop quantum gravity and dynamical triangulations and their main achievements are summarized along with the problems that remain open. Some first attempts to cast string/ \( \mathcal{M} \) theory into a background independent formulation are also mentioned.

The relational/absolute debate has implications also for other issues such as unification and how the parameters of the standard models of physics and cosmology are to be explained. The recent issues concerning the string theory landscape are reviewed and it is argued that they can only be resolved within the context of a background independent formulation. Finally, we review some recent proposals to make quantum theory more relational.

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## Contents

1 Introduction 3

2 A brief history of relational time 6

3 What physicists talk about when we talk about relational space and time 9

4 General relativity is a partly relational theory. 10
4.1 The problem of time and related issues 13

5 Relationalism and the search for the quantum theory of gravity 14
5.1 The causal set theory 16
5.2 Loop quantum gravity 18
5.2.1 Basic results of loop quantum gravity 18
5.2.2 Open problems of loop quantum gravity 20
5.2.3 Lessons from loop quantum gravity for the relational program 21
5.3 Causal dynamical triangulation models 21
5.4 Background independent approaches to string and \( \mathcal{M} \) theory 23

6 Relationalism and reductionism 25
6.1 The challenge of the string theory landscape 29

7 A relational approach to the problems of unification and determination of the standard model parameters 32

8 Relationalism and natural selection 33

9 What about the cosmological constant problem? 35

10 The issue of extending quantum theory to cosmology 36
10.1 Relational approaches to quantum cosmology 37
10.2 Relational approaches to going beyond quantum theory 38

11 Conclusions 39
1 Introduction

During the last three decades research in theoretical physics has focused on four key problems, which, however, remain unsolved. These are

1. The problem of quantum gravity.
2. The problem of further unifying the different forces and particles, beyond the partial unification of the standard model.
3. The problem of explaining how the parameters of the standard models of particles physics and cosmology, including the cosmological constant, were chosen by nature.
4. The problem of what constitutes the dark matter and energy, or whether the evidence for them are to be explained by modifications in the laws of physics at very large scales.

One can also mention a fifth unsolved problem, that of resolving the controversies concerning the foundations of quantum mechanics.

All five problems have remained unsolved, despite decades of determined effort by thousands of extremely talented people. While a number of approaches have been studied, most expectations have been put on string theory as it appears to provide a uniquely compelling unification of physics. Given that the correct perturbative dynamics for gauge fields, fermions and gravitons emerges from a simple action expressed in terms of world-sheets and that, in addition, there are strong indications that the quantum corrections to these processes are finite to each order of string perturbation theory[3], it is hard not to take string theory seriously as a hypothesis about the next step in the unification of physics. At the same time, there remain open problems.

Despite knowing a great deal about the different perturbative string theories and the dualities that relate them, it is widely believed that a more fundamental formulation exists. This would give us a set of equations, solutions to which would give rise to the different perturbative string theories. While there is a lot of evidence for the existence of this more fundamental formulation, in the dualities that relate the different string perturbation theories, there is as yet no agreed upon proposal as to either the principles or the equations of this formulation.

It is also unfortunately the case that the theory makes, as yet, no falsifiable predictions for doable experiments, by which the applicability of the theory to nature could be checked. This is because of the landscape of discrete vacuua which have been uncovered in the last few years. Powerful effective field theory arguments have made it plausible that the theory comes in an infinite number of versions[4]. These appear to correspond to an infinite number of possible universes and low energy phenomenologies. Even if one imposes the minimal phenomenological constraints of a positive vacuum energy and
broken supersymmetry, there are argued to be still a vast ($>10^{300}$) number of theories[5]. There thus appears to be no uniqueness and no predictability so far as observable parameters are concerned, for example, one can get any gauge group and many different spectra of Higgs and fermions.

Of course, these two issues are related. It seems very likely that the challenge posed by the landscape would be resolved if we had a more fundamental formulation of string theory. This would enable us to establish which of the vacua described by effective field theory are truly solutions to the exact theory. It would also allow us to study the dynamics of transformations between different vacua.

Another striking feature of the present situation is that we have no unique predictions for the post-standard model physics which will be explored in upcoming experiments at the LHC. This is true in spite of the fact that we have had three decades since the formulation of the standard model to discover a convincing theory that would give us unique predictions for these experiments. The theory many of our colleagues believe, the supersymmetric extension of the standard model, has too many parameters to yield unique predictions for those experiments.

It is beyond doubt that research in string theory has nonetheless led to a large number of impressive results and conjectures, some of great mathematical beauty. Several mathematical conjectures have been suggested by work in string theory, that turned out to be provable by more rigorous means. A number of interesting conjectures and results have been found for the behavior of supersymmetric gauge theories. All of this suggests that string theory has been worth pursuing. At the same time, the present situation is very far from what was expected when people enthusiastically embraced string theory 20 years ago.

If so much effort has not been rewarded with success, it might be reasonable to ask whether some wrong assumption was made somewhere in the course of the development of the theory. The purpose of this paper is to propose such an hypothesis. This hypothesis is made with an open minded spirit, with the hopes of stimulating discussion.

To motivate my hypothesis, we can start by observing that theorists’ choices of how to approach the key issues in fundamental physics is largely determined by their views on three crucial questions.

- **Must a quantum theory of gravity must be background independent, or can there can be a sensible and successful background dependent approach?**

- **How are the parameters of the standard models of physics and cosmology to be determined?**

- **Can a cosmological theory be formulated in the same language we use for descriptions of subsystems of the universe, or does the extension of physics from local to cosmological require new principles or a new formulation of quantum theory?**

It is the first issue that divides most string theorists from those who pursue alternative approaches to quantum gravity.
The second issue determines the attitude different people take to the landscape. There are, roughly, three possible approaches: 1) a unique theory leading to unique predictions. 2) Anthropic approaches, according to which our universe may be very different from a typical member of an ensemble or landscape of theories. 3) Dynamical, or evolutionary approaches, according to which the dynamics of reproduction of universes results in our universe being a typical member of the ensemble[17]. The first has been, traditionally, the basis of the hopes for a unified theory, but the recent results suggest that unification leads not to a single, unique theory, but a multitude of possible theories. This leaves the other two options.

The third issue has been long appreciated by those who have attempted to formulate a sensible quantum theory of cosmology, but it recently has been raised in the contexts of attempts to resolve the problems of the landscape in terms of cosmological theories and hypotheses.

In this paper I would like to make two observations and an hypothesis about these issues.

- These three debates are closely related and they are unlikely to be resolved separately.
- These three debates are aspects of a much older debate, which has been central to thinking about the nature of space and time going back to the beginning of physics. This is the debate between relational and absolute theories of space and time.

In particular, as I will explain below, background dependent attempts at quantum gravity and anthropic approaches to the landscape are the contemporary manifestations of the absolute side of the old debate. Similarly, background independent approaches to quantum gravity and dynamical or evolutionary approaches to the landscape are firmly within the relational tradition.

Now here is my thesis, which it is the task of this essay to support:

The reason that we do not have a fundamental formulation of string theory, from which it might be possible to resolve the challenge posed by the landscape, is that it has been so far developed as a background dependent theory. This is despite there being compelling arguments that a fundamental theory must be background independent. Whether string theory turns out to describe nature or not, there are now few alternatives but to approach the problems of unification and quantum gravity from a background independent perspective.

This essay is written with the hope that perhaps some who have avoided thinking about background independent theories might consider doing so now. To aid those who

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1A critique of the attempts to resolve the landscape problem through the anthropic principle is given in [6].
might be so inclined, in the next section I give a sketch of how the absolute/relational debate has shaped the history of physics since before the time of Newton. Then, in section 3, I explain precisely what is meant by relational and absolute theories. Section 4 asks whether general relativity is a relational theory and explains why the answer is: partly. We then describe, in section 5, several relational approaches to quantum gravity. There have been some remarkable successes, which show that it is possible to get highly non-trivial results from background independent approaches to quantum gravity[7]. At the same time, there remain open problems and challenges. Both the successes and open problems yield lessons for any future attempt to make a background independent formulation of string theory or any other quantum theory of gravity.

Sections 6 to 8 discuss what relationalism has to offer for the problems in particle physics such as unification and predictability. It is argued that the apparent lack of predictability emerging from studies of the string theory landscape is a symptom of relying on background dependent methodologies in a regime where they cannot offer sensible answers. To support this, I show that relationalism suggests methodologies by which multiverse theories may nevertheless make falsifiable predictions.

Many theorists have asserted that no approach to quantum gravity should be taken seriously if it does not offer a solution to the cosmological constant problem. In section 9 I show that relational theories do offer new possibilities for how that most recalcitrant of issues may be resolved.

Section 10 explores another application of relationalism, which is to the problem of how to extend quantum theory to cosmology. I review several approaches which have been called “relational quantum theory.” These lead to formulations of the holographic principle suitable for quantum gravity and cosmology.

2 A brief history of relational time

The debate about whether space and time are relational is central to the history of physics. Here is a cartoon sketch of the story

Debate about the meaning of motion go back to the Greeks. But the issues of interest for us came into focus when Newton proposed his form of dynamics in his book *Principia Mathematica*, published in 1687. Several of his rough contemporaries, such as Descartes, Huygens and Leibniz espoused relational notions of space and time, according to which space and time are to be defined only in terms of relationships among real objects or events. Newton broke with his contemporaries to espouse an absolute notion of space and time, according to which the geometry of space and time provided a fixed, immutable and eternal background, with respect to which particles moved. Leibniz responded by proposing arguments for a relational view that remain influential to this day

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*A full historical treatment of the relational/absolute debate is in Barbour’s book, [10]*

*Some essential texts, accessible to physicists, are [11].*
Leibniz’s argument for relationalism was based on two principles, which have been the focus of many books and papers by philosophers to the present day. The principle of sufficient reason states that it must be possible to give a rational justification for every choice made in the description of nature. I will refer the interested reader to the original texts[11] for the arguments given for it, but it is not hard to see the relevance of this principle for contemporary theoretical physics. A theory that begins with the choice of a background geometry, among many equally consistent choices, violates this principle. So does a theory that allows some parameters to be freely specified, and allows no mechanism or rational argument why one value is observed in nature.

One circumstance that the principle of sufficient reason may be applied to is spacetimes with global symmetries. Most distributions of matter in such a space will not be invariant under the symmetries. One can then always ask, why is the universe where it is, rather than ten feet to the left, or rotated 30 degrees? Or, why did the universe not start five minutes later? This is sometimes called the problem of under determination: nothing in the laws of physics answers the question of why the whole universe is where it is, rather than translated or rotated.

As there can be no rational answer why the universe is where it is, and not ten feet to the left, the principle of sufficient reason says this question should not arise in the right theory. One response is to demand a better theory in which there is no background spacetime. If all there is to space is an emergent description of relations between particles, questions about whether the whole universe can be translated in space or time cannot arise. Hence, the principle of sufficient reason motivates us to eliminate fixed background spacetimes from the formulation of physical law.

Conversely, if one believes that the geometry of space is going to have an absolute character, fixed in advance, by some a priori principles, you are going to be led to posit a homogeneous geometry. For what, other than particular states of matter, would be responsible for inhomogeneities in the geometry of space? But then spacetime will have symmetries which leave you prey to the argument just given. So from the other side also, we see that the principle of sufficient reason is hard to square with any idea that spacetime has a fixed, absolute character.

One way to formulate the argument against background spacetime is through a second principle of Leibniz, the identity of the indiscernible. This states that any two entities which share the same properties are to be identified. Leibniz argues that were this not the case, the first principle would be violated, as there would be a distinction between two entities in nature without a rational basis. If there is no experiment that could tell the difference between the state in which the universe is here, and the state in which it is translated 10 feet to the left, they cannot be distinguished. The principle says that they must then be identified. In modern terms, this is something like saying that a cosmological theory should not have global symmetries, for they generate motions and charges that could only be measured by an observer at infinity, who is hence not part of the universe. In fact, when we impose the condition that the universe is spatially compact without boundary, general relativity tells us there are no global spacetime symmetries and no
non-zero global conserved charges\textsuperscript{4}. But it took physics a long time to catch up to Leibniz’s thinking. Even if philosophers were convinced that Leibniz had the better argument, Newton’s view was easier to develop, and took off, whereby Leibniz’s remained philosophy. This is easy to understand: a physics where space and time are absolute can be developed one particle at a time, while a relational view requires that the properties of any one particle are determined self-consistently by the whole universe.

Leibniz’s criticisms of Newton’s physics were sharpened by several thinkers, the most influential of which was Mach\textsuperscript{[12]}, who in the late 19th century gave an influential critique of Newtonian physics on the basis of its treatment of acceleration as absolute.

Einstein was among those whose thinking was changed by Mach. There is a certain historical complication, because what Einstein called “Mach’s principle” was not exactly what Mach wrote. But that need not concern us here. The key idea that Einstein got from, or read into, Mach, was that acceleration should be defined relative to a frame of reference that is dynamically determined by the configuration of the whole universe, rather than being fixed absolutely, as in Newton’s theory.

In Newton’s mechanics, the distinction between who is accelerating and who is moving uniformly is a property of an absolute background spacetime geometry, that is fixed independently of the history or configuration of matter. Mach proposed, in essence eliminating absolute space as a cause of the distinction between accelerated and non-accelerated motion, and replacing it with a dynamically determined distinction. This resolves the problem of under-determination, by replacing an a priori background with a dynamical mechanism. By doing this Mach showed us that a physics that respects Leibniz’s principle of sufficient reason is more predictive, because it replaces an arbitrary fact with a dynamically caused and observationally falsifiable relationship between the local inertial frames and the distribution of matter in the universe. This for the first time made it possible to see how, in a theory without a fixed background, properties of local physics, thought previously to be absolute, might be genuinely explained, self-consistently, in terms of the whole universe.

There is a debate about whether general relativity is “Machian”, which is partly due to confusion over exactly how the term is to be applied. But there is no doubt that general relativity can be characterized as a partly relational theory, in a precise sense that I will explain below.

To one schooled in the history of the relational/absolute debate\textsuperscript{5}, it is easy to understand the different choices made by different theorists as reflecting different expectations.

\textsuperscript{4}That is, special solutions may have symmetries. But, as we will discuss in section 4, there are no symmetries acting on the space of physical solutions of the theory, once these have been identified with equivalence classes under diffeomorphisms\textsuperscript{[56]}.

\textsuperscript{5}The understanding that working physicists like myself have of the relevance of the relational/absolute debate to the physical interpretation of general relativity and contemporary efforts towards quantum gravity is due mainly to the writings and conference talks of a few physicists—primarily John Stachel\textsuperscript{[8]} and Julian Barbour\textsuperscript{[9]}. Also important were the efforts of philosophers who, beginning in the early 90’s were kind enough to come to conferences on quantum gravity and engage us in discussion.
and understandings of that debate[13]. The same can be said about the debates about the merits of the Anthropic Principle as a solution to the very puzzling situation that string theory has found itself in recently[6]. To explain why, we need some precise definitions.

3 What physicists talk about when we talk about relational space and time

While many physicists have been content to work with background dependent theories, from the earliest attempts at quantum gravity there has been a community of those who shared the view that any approach must be background independent. Among them, there has been a fair amount of discussion and reflection concerning the roots of the notion of background independence in older relational views of space and time. From this has emerged a rough consensus as to what may be called the physicists’ relational conception of space and time^6.

Any theory postulates that the world is made up of a very large collection of elementary entities (whether particles, fields, or events or processes.) Indeed, the fact that the world has many things in it is essential for these considerations—it means that the theory of the world may be expected to differ in important aspects from models that describe the motion of a single particle, or a few particles in interaction with each other.

The basic form of a physical theory is framed by how these many entities acquire properties. In an absolute framework the properties of any entity are defined with respect to a single entity—which is presumed to be unchanging. An example is the absolute space and time of Newton, according to which positions and motions are defined with respect to this unchanging entity. Thus, in Newtonian physics the background is three dimensional space, and the fundamental properties are a list of the positions of particles in absolute space as a function of absolute time: \( x_i^a(t) \). Another example of an absolute background is a regular lattice, which is often used in the formulation of quantum field theories. Particles and fields have the property of being at different nodes in the lattice, but the lattice does not change in time.

The entities that play this role may be called the background for the description of physics. The background consists of presumed entities that do not change in time, but which are necessary for the definition of the kinematical quantities and dynamical laws.

The most basic statement of the relational view is that

**R1** *There is no background.*

How then do we understand the properties of elementary particles and fields? The relational view presumes that

^6Philosophers distinguish several versions of relationalism[14], among which, what is described here is what some philosophers call *eliminative relationalism.*
The fundamental properties of the elementary entities consist entirely in relationships between those elementary entities.

Dynamics is then concerned with how these relationships change in time.

An example of a purely relational kinematics is a graph. The entities are the nodes. The properties are the connections between the nodes. The state of the system is just which nodes are connected and which are not. The dynamics is given by a rule which changes the connectivity of the graph.

We may summarize this as

The relationships are not fixed, but evolve according to law. Time is nothing but changes in the relationships, and consists of nothing but their ordering.

Thus, we often take background independent and relational as synonymous. The debate between philosophers that used to be phrased in terms of absolute vs relational theories of space and time is continued in a debate between physicists who argue about background dependent vs background independent theories.

It should also be said that for physicists relationalism is a strategy. As we shall see, theories may be partly relational, i.e. they can have varying amounts of background structure. One can then advise that progress is achieved by adopting the

Relational strategy: Seek to make progress by identifying the background structure in our theories and removing it, replacing it with relations which evolve subject to dynamical law.

Mach’s principle is the paradigm for this strategic view of relationalism. As discussed above, Mach’s suggestion was that replacing absolute space as the basis for distinguishing acceleration from uniform motion with the actual distribution of matter would result in a theory that is more explanatory, and more falsifiable. Einstein took up Mach’s challenge, and the resulting success of general relativity can be taken to vindicate both Mach’s principle and the general strategy of making theories more relational.

4 General relativity is a partly relational theory.

We begin a more detailed discussion with general relativity. As I will describe, general relativity can be characterized as a partly relational theory. As such, it serves as a good example of the power of the relational strategy.

There is one clarification that should be stated at the outset: the issue of whether general relativity is Machian or relational is only interesting if we take general relativity as a possible cosmological theory. This means that we take the spatial topology to be compact, without boundary. In some models of subsystems of the universe, one does not do this. In these cases space has a boundary and one has to impose conditions on the metric and fields at the boundary. These boundary conditions become part of the background, as they indicate that there is a region of spacetime outside of the dynamical
There is of course nothing wrong with modeling sub-systems of the universe with boundaries on which we impose boundary conditions. One way to do this is to assume that the system under study is isolated, so that as one moves away from it the spacetime satisfies asymptotic conditions. But the boundary or asymptotic conditions can only be justified by the assertion that the system modeled is a subsystem of the universe. No fundamental theory could be formulated in terms that require the specification of boundary or asymptotic conditions because those conditions imply that there is a part of the universe outside of the region being modeled. Thus, one cannot assert that a theory defined only with the presence of such conditions can be fundamental.

But at the same time, the fact that asymptotic conditions can be imposed does not mean general relativity is not fundamental, since it can also be formulated for cosmologies by making the universe compact without boundary. It does mean that it is only interesting to ask if general relativity is a relational theory in the cosmological case.\(^7\)

General relativity is a complicated theory and there has been a lot of confusion about it. However, I will show now why it is considered to be mainly, but not purely, a relational theory. One reason it is complicated is that there are several layers of structure.

- Dimension
- Topology
- Differential structure
- Signature
- Metric and fields

We denote a spacetime by \((M, g_{ab}, f)\), where \(M\), refers to the first four properties, \(g_{ab}\) is the metric and \(f\) stands for all the other fields.

It is true that in general relativity the dimension, topology, differential structure and signature are fixed. They can be varied from model to model, but they are arbitrary and not subject to law. These do constitute a background.\(^8\)

Then why do we say the theory is relational? Given this background, we can define an equivalence relation called a diffeomorphism. A diffeomorphism \(\phi\) is a smooth, invertible map from a manifold to itself.\(^9\)

\[
\phi(M, g_{ab}, f) \rightarrow (M', g'_{ab}, f')
\]

\(^7\)But it is worth asking whether the fact that GR allows models with boundary conditions means that it is incomplete, as a fundamental theory.

\(^8\)A very interesting question is whether the restriction to fixed dimension and topology is essential or may be eliminated by a deeper theory.

\(^9\)More generally to another manifold.
which takes a point $p$ to another point $\phi \cdot p$, and drags the fields along with it by

$$ (\phi \cdot f)(p) = f(\phi^{-1} \cdot p) $$

(2)

The diffeomorphisms of a manifold constitute a group, $Diff(M)$, called the group of diffeomorphisms of the manifold. The basic postulate, which makes GR a relational theory is

**R4** A physical spacetime is defined to correspond, not to a single $(M, g_{ab}, f)$, but to an equivalence class of manifolds, metrics and fields under all actions of $Diff(M)$. This equivalence class may be denoted $\{M, g_{ab}, f\}$.

The important question for physics is what information is coded inside an equivalence class $\{M, g_{ab}, f\}$, apart from the information that is put into the specification of $M$?

The key point is that the points and open sets that define the manifold are not preserved under $Diff(M)$, because any diffeomorphism except the identity takes points to other points. Thus, the information coded in the equivalence classes cannot be described simply as the values of fields at points.

The answer is that

1) Dimension and topology are coded in $\{M, g_{ab}, f\}$

2) Apart from those, all that there is, is a system of relationships between events. Events are not points of a manifold, they are identifiable only by coincidences between the values of fields preserved by the actions of diffeomorphisms.

The relations between events are of two kinds

- **causal order** (i.e. which events causally precede which, given by the lightcone structure).

- **measure** (The spacetime volumes of sets defined by the causal order.)

It can be shown that the information in a spacetime $\{M, g_{ab}, f\}$ is completely characterized by the causal structure and the measure[15]. Intuitively, this is because the conformal metric\textsuperscript{10} determines, and is determined by, the light cones and hence the causal structure. The remaining conformal factor then determines the volume element.

The problem of problem of under-determination raised in section 2 is solved by the identification, in **R4**, of physical histories with equivalence classes. For the spatially compact case, once we have moded out by the diffeomorphisms, there remain no symmetries on the space of solutions[56]. But why should we mod out by diffeomorphisms? As Einstein intuited in his famous “hole argument”, and Dirac codified, one must mod out by diffeomorphisms if one is to have deterministic evolution from initial data[8, 13, 38].

This establishes that, apart from the specification of topology, differential structure and dimension, general relativity is a relational physical theory.

\textsuperscript{10}Defined as the equivalence class of metrics related by local conformal transformations $g_{ab} \rightarrow g'_{ab} = \phi^2 g_{ab}$, where $\phi$ is a function.
4.1 The problem of time and related issues

As I emphasized at the beginning of this section, a truly fundamental theory cannot be formulated in terms of boundaries or asymptotic conditions. This, together with diffeomorphism invariance, implies that the hamiltonian is a linear combination of constraints. This is no problem for defining and solving the evolution equations, but it does lead to subtleties in the question of what is an observable. One important consequences is that one cannot define the physical observables of the theory without solving the dynamics. In other words, as Stachel emphasizes, there is no kinematics without dynamics. This is because all observables are relational, in that they describe relations between physical degrees of freedom. You cannot just ask what is happening at a manifold point, or an event, labeled by some coordinate, and assume you are asking a physically meaningful question. The problem is that because of diffeomorphism invariance, points are not physically meaningful without a specification of how a point or event is to be identified by the values of some physical degrees of freedom. As a result, even observables that refer to local points or regions of physical spacetime are non-local in the sense that as functions of initial data they depend on data in the whole initial slice.

As a result, the physical interpretation of classical general relativity is more subtle than is usually appreciated. In fact, most of what we think we understand naively about how to interpret classical GR applies only to special solutions with symmetries, where we use the symmetries to define special coordinates. These methods do not apply to generic solutions, which have no symmetries. It is possible to give a physical interpretation to the generic solutions of the theory, but only by taking into account the issues raised by the facts that all physical observables must be diffeomorphism invariant, and the related fact that the hamiltonian is a sum of constraints.

We see here a reflection of Leibniz’s principles, in that the interpretation that must be given to generic solutions, without symmetries, is completely different from that given to the measure zero of solutions with symmetries.

One can actually argue something stronger: Suppose that one could transform general relativity into a form in which one expressed the dynamics directly in terms of physical observables. That is, observables which commute with all the constraints, but still measure local degrees of freedom. Then the solutions with symmetries might just disappear. This is because, being diffeomorphism invariant, such observables can distinguish points only by their having different values of fields. Such observables must degenerate when one attempts to apply them to solutions with symmetries. Thus, expressed in terms of generic physical observables, there may be no symmetric solutions. If this is true this would be a direct realization of the identity of the indiscernible in classical general relativity.

Thus, even at the classical level, there is a distinction between background independent and background dependent approaches to the physical interpretation. If one is interested only in observables for particles moving within a given spacetime, one can use a

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11This is reviewed in [38, 16].
construction that regards that spacetime as fixed. But if one wants to discuss observables of the gravitational field itself, one cannot use background dependent methods, for those depend on fixing the gravitational degrees of freedom to one solution. To discuss how observables vary as we vary the solution to the Einstein equations we need functions of the phase space variables that make sense for all solutions. Then one must work on the full space of solutions, either in configuration space or phase space.

One can see this with the issue of time. If by time you mean time experienced by observers following worldlines in a given spacetime, then we can work within that spacetime. For example, in a given spacetime time can be defined in terms of the causal structure. But if one wants to discuss time in the context in which the gravitational degrees of freedom are evolving, then one cannot work within a given spacetime. One constructs instead a notion of time on the infinite dimensional phase or configuration space of the gravitational field itself. Thus, at the classical level, there are clear solutions to the problems of what is time and what is an observable in general relativity.

Any quantum theory of gravity must address the same issues. Unfortunately, background dependent approaches to quantization evade these issues, because they take for granted that one can use the special symmetries of the non-dynamical backgrounds to define physical observables. To usefully address issues such as the problem of time, or the construction of physical observables, in a context that includes the quantum dynamics of the spacetime itself, one must work in a background independent formulation.

However, while the problem of time has been addressed in the context of background independent approaches to quantum gravity, the problem has not been definitively solved. The issue is controversial and there is strong disagreement among experts. Some believe the problem is solved, at least in principle, by the application of the same insights that lead to its solution in classical general relativity[38]. Others believe that new ideas are needed[16]. While I will not dwell on it here, the reader should be aware that the problem of time is a key challenge that any complete background independent quantum theory of gravity must solve.

5 Relationalism and the search for the quantum theory of gravity

Let us begin by noting that conventional quantum theories are background dependent theories. The background structures for a quantum theory include space and time, either Newtonian or in the case of QFT, some fixed, background spacetime. There are additional background structures connected with quantum mechanics, such as the inner product. It is also significant that the background structures in quantum mechanics are connected to the background space and time. For example, the inner product codes probability conservation, in a given background time coordinate.

Thus, when we attempt to unify quantum theory with general relativity we have to face the question of whether the resulting theory is to be background dependent or not.
There are two kinds of approaches, which take the two possible answers-yes and no. These are called background independent and background dependent approaches.

Background dependent approaches study quantum theory on a background of a fixed classical spacetime. These can be quantum theories of gravity in a limited sense in which they study the quantization of gravitational waves defined as moving (to some order of approximation) on a fixed background spacetime. One splits the metric into two pieces

$$g_{ab} = b_{ab} + h_{ab}$$

where $b_{ab}$ is the background metric, a fixed solution to the Einstein equations, and $h_{ab}$ is a perturbation of that solution. In a background dependent approach one quantizes $h_{ab}$ using structures that depend on the prior specification of $b_{ab}$, as if $h_{ab}$ were an ordinary quantum field, or some substitute such as a string.

Background dependent approaches include

- perturbative quantum general relativity
- string theory.

Perturbative quantum general relativity does not lead to a good theory, nor are the problems cured by modifying the theory so as to add supersymmetry or other terms to the field equations.

It is hard to imagine a set of better motivated conjectures than those that drove interest in string theory. Had string theory succeeded as a background dependent theory, it would have served as a counter-argument to the thesis of this essay\(^{12}\). Conversely, given that the problems string theory faces seem deeply rooted in the structure of the theory, it may be worthwhile to examine the alternative, which is background independent theories.

In recent years there has been healthy development of a number of different background independent approaches to quantum gravity. These include,

- Causal sets
- Loop quantum gravity (or spin foam models)
- Dynamical triangulations models.
- Certain approaches to non-commutative geometry\[^{23} \].
- A number of approaches that posit a fundamental discrete quantum theory from which classical spacetime is conjectured to emerge at low energies\[^{22} \].
- Attempts to formulate string theory as a background independent theory.

I will briefly describe the first three. These are well enough understood to illustrate both the strengths of the relational view for quantum gravity and the hard issues that any such approach must overcome.

\(^{12}\)A more detailed summary of the results achieved in string theory and other approaches to quantum gravity, together with a list of problems that remain unsolved is given in [2].
5.1 The causal set theory

To describe the causal set model we need the definition of a causal set.

A causal set is a partially ordered set such that the intersection of the past and future of any pair of events is a finite set. The elements of the causal set are taken to be physical events and their partial ordering is taken to code the relation of physical causation.

The basic premises of the causal set model are[24]

1) A history of the universe consists of nothing but a causal set. That is, the fundamental events have no properties except their mutual causal relations\(^{13}\).

2) The quantum dynamics is defined by assigning to each history a complex number which is to be its quantum amplitude\(^ {14}\).

The motivation for the causal set hypothesis comes from the expectation that the geometry of spacetime becomes discrete at the Planck scale. This leads one to expect that, given any classical spacetime \(\{M, g_{ab}\}\), one will be able to define a causal set \(C\) which approximates it. The precise sense in which this is possible is:

We say that a causal set \(C\) approximates a classical spacetime, \(\{M, g_{ab}, f\}\), if, to each event \(e\) in \(C\) there is an event \(e\) in \(\{M, g_{ab}, f\}\), such that 1) the causal relations are preserved and 2) there is on average 1 event \(e\) coming from \(C\) per Planck volume of \(\{M, g_{ab}, f\}\).

We note that when a causal set does approximate a classical spacetime, it does so because it is the result of a fair sampling of the relations that define the spacetime, which are the causal order and measure.

However if the discrete quantum theory is to be more fundamental there should be a procedure to define the classical spacetime \(\{M, g_{ab}, f\}\) from some kind of classical or low energy limit of the causal set theory. This has not yet been achieved. A main reason is the following problem, which we call the inverse problem for causal sets\(^ {19}\).

The inverse problem for causal sets: Given a classical spacetime \(\{M, g_{ab}, f\}\), it is easy to define a causal set \(C\) which approximates it in the sense just defined. But almost no causal set \(C\) approximates a low dimensional manifold in this sense. Moreover, we do not have a characterization, expressed only in terms of the relations in a causal set, \(C\), which would allow us to pick out those causal sets that do approximation spacetimes. We can only do this by first constructing classical spacetimes, and then extracting from them a causal set that approximates them. Moreover no dynamical principle has been discovered which would generate causal sets \(C\) that either directly approximate low dimensional classical spacetimes, or have coarse grainings or approximations that do so.

\(^{13}\)The events of a causal set are sometimes called “elements” to emphasize the principle that each corresponds to a finite element of spacetime volume.

\(^{14}\)In the causal set literature the dynamics is sometimes formulated in terms of quantum measure theory, which is a variant of the consistent histories formulation of quantum mechanics.
This is an example of a more general class of problems, which stems from the fact that combinatorially defined discrete structures are very different from continuous manifolds. A very general combinatorial structure is a graph. The possibility of a correspondence between a graph and a smooth geometry is based on two definitions.

**Definition:** The metric on a graph $\Gamma$ is defined by $g(j, k)$ for two nodes $k$ and $j$ is the minimal number of steps to walk from $j$ to $k$ along the graph.

**Definition:** A graph $\Gamma$ is said to approximate a manifold and metric $\{M, g_{ab}\}$ if there is an embedding of the nodes of $\Gamma$ into points of $\{M, g_{ab}\}$ such that the graph distance $g(j, k)$ is equal to the metric distance between the images of the nodes in $\{M, g_{ab}\}$.

It is easy to see that the following issue confronts us.

**Inverse problem for graphs.** Given any $\{M, g_{ab}\}$ it is easy to construct a graph $\Gamma$ that approximates it. But, assuming only that the dimension is much less than the number of nodes, for almost no graphs do there exist low dimensional smooth geometries that they approximate.

Because of the inverse problem, it is fair to say that the causal set program has unfortunately so far failed to lead to a good physical theory of quantum gravity. But it is useful to review the logic employed:

**Logic of the causal set program:**
- GR is relational, and the fundamental relations are causal relations.
- But GR is continuous and it is also non-quantum mechanical
- We expect that a quantum theory of spacetime should tell us the set of physical events is discrete.
- Therefore a quantum spacetime history should consist of a set of events which is a discrete causal structure.
- Moreover, the causal structure is sufficient to define the physical classical spacetime, so it should be sufficient to describe a fundamental quantum history.
- But this program so far fails because of the inverse problem.

Given the seriousness of the inverse problem, it is possible to imagine that the solution is that there are more fundamental relations, besides those of causality. It should be said that this direction is resisted by some proponents of causal sets, who are rather “purist” in their belief that the relation of causality is sufficient to constitute all of physics. But a possible answer to this question is given by another program, loop quantum gravity, where causal relations are local changes in relational structures that describe the quantum geometry of space[20].

17
5.2 Loop quantum gravity

Loop quantum gravity was initiated in 1986 and is by now a well developed research program, with on the order of 100 practitioners. There is now a long list of results, many of them rigorous. Here I will briefly summarize the key results that bear on the issue of relational space and time\textsuperscript{15}.

5.2.1 Basic results of loop quantum gravity

Loop quantum gravity is based on the following observation, introduced by Sen and Ashtekar for general relativity and extended to a large class of theories including general relativity and supergravity in spacetime dimensions three and higher\textsuperscript{16}.

- General relativity and supergravity, in any spacetime dimension greater than or equal to $2 + 1$, can be rewritten as gauge theories, such that the configuration space is the space of a connection field, $A_a$, on a spatial manifold $\Sigma$. The metric information is contained in the conjugate momenta. The gauge symmetry includes the diffeomorphisms of a spacetime manifold, usually taken to be $\Sigma \times \mathbb{R}$. The dynamics takes a simple form that can be understood as a constrained topological field theory. This means that the action contains one term, which is a certain topological field theory called $BF$ theory, plus another term which generates a quadratic constraint.

Consider such a classical gravitational theory, $T$, whose histories are described as diffeomorphism equivalence class of connections and fields, $\{M, A_a, f\}$. To define the action principle one must assume that the topology, dimension and differential structure of spacelike surfaces, $\Sigma$, are fixed.

The following results have then been proven\textsuperscript{7}:

1. The quantization of $T$ results in a unique Hilbert space, $H$ of diffeomorphism invariant states. There is a recent uniqueness theorem\textsuperscript{25}, which guarantees that for dimension of $\Sigma$ two or greater, there is a unique quantization of a gauge field such that i) the Wilson loops are represented by operators that create normalizable states, ii) its algebra with the operator that measures electric field flux is represented faithfully and iii) the diffeomorphisms of $\Sigma$ are unitarily implemented without anomaly.

This unique Hilbert space has a beautiful description. There is a orthonormal basis of $H$ whose elements are in one to one correspondence with the embeddings of certain labeled graphs $\Gamma$ in $\Sigma$. (The label set varies depending on the dimension, matter fields, and with supersymmetry.)

Because $H$ carries a unitary representation of $Diff(\Sigma)$ it is possible rigorously to mod out by the action of diffeomorphisms and construct a Hilbert space, $H^{diff}$ of

\textsuperscript{15}For details of the results, including those mentioned below, and references, see [7]. Books on loop quantum gravity include [37, 38] and review papers include [39].

\textsuperscript{16}See for example, [40] and [7] and references contained therein.
spatially diffeomorphism invariant states. This has a normalizable basis in one to one correspondence with the diffeomorphism classes of the embeddings in $\Sigma$ of the labeled graphs.

This is a very satisfactory description from the point of view of relationalism. There is no more relational structure than a graph, as two nodes are distinguished only by their pattern of connections to the rest of the graph. The labels come from the theory representations of a group or algebra $\mathcal{A}$. The edges are labeled by representations of $\mathcal{A}$, which describe properties shared between the nodes they connect. The labels on nodes are invariants of $\mathcal{A}$, which likewise describe properties shared by the representations on edges incident on those nodes.

Because there is a background topology, there is additional information coded in how the edges of the graph knot and link each other. Given the choice of background topology, this information is also purely relational.

2. A quantum history is defined by a series of local moves on graphs that take the initial state to the final state[20]. The set of local moves in each history define a causal set.

Hence, the events of the causal set arise from local changes in another set of relations, that which codes the quantum geometry of a spatial slice. The structure that merges the relational structure of graphs with that of causal sets is now called a causal spin foam.

3. The amplitudes for local moves that follow from the quantization of the Einstein equations are known in closed form. The sums over those amplitudes are known to be ultraviolet finite. Similarly, the quantum Einstein equations in the Hamiltonian form have been implemented by exact operator equations on the states.

In the case of a spin foam model for $2+1$ gravity coupled to massive particles, it has been shown in detail that the theory can be re-summed, yielding an effective field theory on a non-commutative spacetime[21]. This provides an explicit demonstration of how physics in classical spacetime can emerge from a non-trivial background independent quantum theory of gravity. The resulting effective field theory has in addition deformed Poincare symmetry, which confirms, in this case, the general conjecture that the low energy limit of loop quantum gravity has deformed Poincare symmetry[7].

4. The quantum spacetime is discrete in that each node of the graph corresponds to a finite quanta of spatial volume. The operators that correspond to volumes, areas and lengths are finite, and have discrete spectra with finite non-zero minimal values. Hence a graph with a finite number of nodes and edges defines a region of space with finite volume and area.
5. There are a number of robust predictions concerning subjects like black hole entropy. Evidence has recently been found that both cosmological and black hole singularities bounce, so the evolution of the universe continues through apparent classical cosmological singularities.

6. There are explicit constructions of semiclassical states, coarse grained measurements of which reproduce classical geometries. Excitations of these states, with wavelengths long in Planck units, relative to those classical geometries, have been shown to reproduce the physics of quantum fields and linearized gravitational waves on those backgrounds.

5.2.2 **Open problems of loop quantum gravity:**

There are of course many, in spite of the fact that the theory is well defined.

- **Classical limit problem:** Find the ground state of the theory and show that it is a semiclassical state, excitations of which quantum field theory and classical GR.

- **Do science problem:** By studying the excitations of semiclassical states, make predictions for doable experiments that can test the theory up or down.

- **Remove the remaining background dependence problem:** The results so far defined depend on the fact that the dimension and topology of the spatial manifold, $\Sigma$, is fixed, so that the graphs are embedded in $\Sigma$. This helps by lessening the inverse problem. Can this be removed—and the inverse problem solved—so that all the structure that was background for previous theories, including dimension and topology, is explained as following from solutions to a relational theory\(^\text{17}\)?

  We note that in some formulations of spin foam models, the dependence on a fixed background topology is dropped, so that the states and histories are defined as pure combinatorial structures. But this makes the problem of recovering classical general relativity from the low energy limit more complicated.

- **The problem of time:** The different proposals that have been made to resolve the problem of time in quantum gravity and cosmology can all be studied in detail in loop quantum gravity and related cosmological models. While there are some interesting results, the opinion of this author is that the problem remains open.

  These are hard problems, and remain unsolved, but some progress is being made on all of them.

  It is important to mention that there are real possibilities for experimental tests of the theory. This is because the discrete structure of space and time implies modifications in the usual relations between energy and momenta

\[
E^2 = p^2 + m^2 + l_p E^3 + ... \tag{4}
\]

\(^{17}\)For more on the inverse problem and its implications, see [19].
This turns out to have implications for experiments currently underway, having to do with ultra high energy cosmic rays and gamma ray bursts, amongst others\textsuperscript{18}. Loop quantum gravity appears to make predictions for these experiments\textsuperscript{[41]}.

5.2.3 Lessons from loop quantum gravity for the relational program

So far as the relational/absolute debate is concerned, loop quantum gravity teaches us several lessons:

- So long as we keep as background those aspects of space and time that are background for classical GR, (the topology, dimension and differential structure), we can find a quantum mechanical description of the metric and fields. Thus LQG is partly relational, in exactly the same way that GR is partly relational.

- Loop quantum gravity does give us a detailed description of quantum spatial and spacetime geometry. There are many encouraging results, such as finiteness, and the derivation of an explicit language of states, histories, and observables for general background independent theories of quantum gravity. It is possible to do non-trivial computations to study the dynamics of quantum spacetime, and applications to physical problems such as black holes and cosmology yield results that are sensible and, in some cases, testable. It is very satisfying that the description of quantum geometry and quantum histories are formulated using beautiful relational structures such as graphs and causal sets.

- This description is flexible and can accommodate different hypotheses as to the dimension of spacetime, matter couplings, symmetries and supersymmetries.

- There do remain hard open problems having to do with how a classical spacetime is to emerge from a purely background independent description. A related challenge is to convincingly resolve the problem of time. Nevertheless, significant progress is being made on these problems\textsuperscript{[21]}, and it even appears to be possible to derive predictions for experiment by expanding around certain semiclassical states\textsuperscript{[41]}.

- The main barrier to making an entirely relational theory of quantum spacetime appears to be the inverse problem.

5.3 Causal dynamical triangulation models

These are models for quantum gravity, based on a very simple construction\textsuperscript{[26]-[32]}. A quantum spacetime is represented by a combinatorial structure, which consists of a large number \(N\) of \(d\) dimensional simplexes (triangles for two dimensions, tetrahedra for three etc.) glued together to form a discrete approximation to a spacetime. Each such discrete

\textsuperscript{18}See [7] for a brief review of this important subject, with additional references.
spacetime is given an amplitude, which is gotten from a discrete approximation to the action for general relativity. Additional conditions are imposed, which guarantee that the resulting structure is the triangulation of some smooth manifold (otherwise there is a severe inverse problem.) For simplicity the edge lengths are taken to be all equal to a fundamental scale, which is considered a short distance cutoff\(^9\) One defines the quantum theory of gravity by a discrete form of the sum over histories path integral, in which one sums over all such discrete quantum spacetimes, each weighed by its amplitude.

These models were originally studied as an approach to Euclidean quantum gravity (that is the path integral sums over spacetimes with Euclidean signature, rather than the Lorentzian signature of physical spacetime.) In these models the topology is not fixed, so one has a model of quantum gravity in which one can investigate the consequences of removing topology from the background structure and making it dynamical[26].

More recently, a class of models have been studied corresponding to Lorentzian quantum gravity. In these cases additional conditions are fixed, corresponding to the existence of a global time slicing, which restricts the topology to be of the form of \(\Sigma \times \mathbb{R}\), where \(\Sigma\) is a fixed spatial topology[27]\(^\text{20}\).

Some of the results relevant for the debate on relationalism include,

- In the Euclidean case, for spacetime dimensions \(d > 2\), the sum over topologies cannot be controlled. The path integral is, depending on the parameters of the action chosen, unstable to the formation of either an uncontrolled spawning of “baby universes”, or to a crunch down to degenerate triangulations. Neither converges to allow a coarse grained approximation in terms of smooth manifolds of any dimension.

- In the Lorentzian case, when the simplices have spacetime dimension \(d = 2, 3, 4\), where the topology is fixed and the formation of baby universes suppressed, there is evidence for convergence to a description of physics in manifolds whose macroscopic dimension is the same as the microscopic dimension. For the case of \(d = 4\) there results are recent and highly significant[27, 28]. In particular, there is now detailed numerical evidence for the emergence of \(3+1\) dimensional classical spacetime at large distances from a background independent quantum theory of gravity[28].

- The measure of the path integral is chosen so that each triangulation corresponds to a diffeomorphism class \(\{M, g_{ab}, f\}\). The physical observables such as correlation functions measured by averaging over the triangulations correspond to diffeomorphism invariant relational observables in spacetime.

These results are highly significant for quantum gravity. It follows that earlier conjectures about the possibility of defining quantum gravity through the Euclidean path

\(^{19}\)There is a different, but related approach, called Regge calculus, in which the triangulations are fixed while the edge lengths are varied.

\(^{20}\)The condition of a fixed global time slicing can be relaxed to some extent[29]
integral cannot be realized. The sum has to be done over Lorentzian spacetimes to have a hope of converging to physics that has a coarse grained description in smooth space-times. Further, earlier conjectures about summing over topologies in the path integral also cannot be realized.

As far as relationalism is concerned we reach a similar conclusion to that of loop quantum gravity. There is evidence for the existence of the quantum theory when structures including topology, dimension and signature are fixed, as part of the background structure, just as they are in classical general relativity. When this is done one has a completely relational description of the dynamics of a discrete version of metric and fields. Furthermore, in the context of each research program there has recently been reported a detailed study showing of how classical spacetime emerges from an initially discrete, background independent theory. This is an analytic result in the case of spin foam models in $2 + 1$ dimensions, with matter\cite{21}, and numerical results in $3 + 1$ dimensions in the causal dynamical triangulations case\cite{27, 28}. This is very encouraging, given that the problem of how classical spacetime emerges is the most challenging problem facing background independent approaches to quantum gravity.

5.4 Background independent approaches to string and M theory

It has been often argued that string theory requires a background independent formulation. This is required, not just because any quantum theory of gravity must be background independent, but because there is a need to unify all the different perturbative string theories into one theory. As this must combine theories defined on different backgrounds, it must not be restricted by the choice of a particular background.

There are some claims that string theory does not need a background independent formulation, and can be instead defined for fixed boundary or asymptotic conditions as dual to a field theory on a fixed background, as in the AdS/CFT correspondence. To respond to this, it first should be emphasized that the considerable evidence in favor of some form of an AdS/CFT correspondence falls short of a proof of actual equivalence, which would be needed to say that a full quantum theory of gravity, rather than just limits of correlation functions taken to the boundary, is coded in the dual conformal field theory \cite{33, 2}). But even granting the full Maldacena conjecture it is hard to see how a theory defined only in the presence of boundary or asymptotic conditions, as interesting as that would be, could be taken as a candidate for a complete formulation of a fundamental theory of spacetime. This is because the boundary or asymptotic conditions can only be interpreted physically as standing for the presence of physical degrees of freedom outside the theory. For example, the timelike or null killing fields at the boundary stand for the reading of a clock which is not part of the physical systems. Such a formulation cannot be applied to cosmological problems, where the problem is precisely to formulate a consistent theory of the entire universe as a closed system. General relativity with spatially compact boundary conditions is such a theory. Hence, it seems reasonable to require that a quantum theory of gravity, which is supposed to reproduce general relativity, must also make
sense as a theory of a whole universe, as a closed system.

Some string theorists have also claimed that string theory does not need a background independent formulation, because the fact that string perturbation theory is, in principle, defined on many different backgrounds is sufficient. This assertion rests on exaggeration and misunderstanding. First, string perturbation theory is so far only defined on stationary backgrounds that have timelike killing fields. But this is a measure zero of solutions to the Einstein equations. It is, however, difficult to believe that a consistent string perturbation theory can be defined on generic solutions to the Einstein equations because, in the absence of timelike killing fields, one cannot have spacetime supersymmetry, without which the spectrum will generally contain a tachyon\(^{21}\).

More generally, this assertion misses completely the key point that general relativity is itself a background independent theory. Although we sometimes use the Einstein’s equations as if they were a machine for generating solutions, within which we then study the motion of particles of fields, this way of seeing the theory is inadequate as soon as we want to ask questions about the gravitational degrees of freedom, themselves. Once we ask about the actual local dynamics of the gravitational field, we have to adopt the viewpoint which understands general relativity to be a background independent theory within which the geometry is completely dynamical, on an equal footing with the other degrees of freedom. The correct arena for this physics is not a particular spacetime, or even the linearized perturbations of a particular spacetime. It is the infinite dimensional phase space of gravitational degrees of freedom. From this viewpoint, individual spacetimes are just trajectories in the infinite dimensional phase or configuration space; they can play no more of a role in a quantization of spacetime than a particular classical orbit can play in the quantization of an electron.

To ask for a background independent formulation of string theory is to ask only that it conserve the fact that the dynamics of the Einstein equations does not require, indeed does not allow, the specification of a fixed background metric. For, if one means anything at all by a quantum theory of gravity, one certainly means a theory by which the degrees of freedom of the classical theory emerge from a suitable limit of a Hilbert space description. This does not commit oneself to the belief that the elementary degrees of freedom are classical metrics or connections, nor does it commit oneself to a belief that the correct microscopic dynamics have to do with the Einstein equations. But it does imply that a quantum theory must have a limit in which it reproduces the correct formulation of general relativity as a dynamical system, which is to say in the background independent language of the classical phase space. It would seem very unlikely that such a background independent formulation can emerge as a classical limit of a theory defined only on individual backgrounds, which are just trajectories in the exact phase space.

In fact, there have been a few attempts to develop a background independent approach to string and \(\mathcal{M}\) theory\([35, 36]\). These have been based on two lessons from loop quantum gravity: i) Background independent quantum theories of gravity can be based

\(^{21}\)Note that for none of the theories in the landscape is it known how to construct the free string worldsheet theory.
on matrix models, so long as their formulation depends on no background metric. Such a model can be based on matrices valued in a group, as in certain formulations of spin foam models. ii) The dynamics of all known gravitational theories can be understood by beginning with a topological field theory and then extending the theory so as to minimally introduce local degrees of freedom. This can be extended to supergravity, including the 11-dimensional theory[34].

By combining these, a strategy was explored in which a background independent formulation of string or $M$ theory was to be made which is an extension of a matrix Chern-Simons theory[35]. The Chern-Simons theory provides a starting point which may be considered a membrane dynamics, but without embedding in any background manifold. The background manifold and embedding coordinates then arise from classical solutions to the background independent membrane model. It was then found that background dependent matrix models of string and $M$ theory emerged by expanding around these classical solutions.

A recent development in this direction is a proposal for how to quantize a certain reduction of $M$ theory non-perturbatively[36].

These few, preliminary, results, indicate that it is not difficult to invent and study hypotheses for background independent formulations of string theory.

6 Relationalism and reductionism

I would now like to broaden the discussion by asking: Does the relational view have implications broader than the nature of space and time? I will argue that it does$^{22}$. A starting point for explaining why is to begin with a discussion of reductionism.

To a certain degree, reductionism is common sense. When a system has parts, it makes sense to base an understanding of it on the laws that the parts satisfy, as well as on patterns that emerge from the exchanges of energy and information among the parts. In recent years we have learned that very complex patterns can emerge when simple laws act on the parts of a system, and this has led to the development of the study of complex systems. These studies have shown that there are useful principles that apply to such complex systems and these may help us to understand an array of systems from living cells to ecosystems to economic systems. But this is not in contradiction to reductionism, it is rather a deepening of it.

But there is a built in limit to reductionism. If the properties of a complex system can be understood in terms of their parts, then we can keep going and understanding the parts in terms of their parts, and so on. We can keep looking at parts of parts until we reach particles that we believe are elementary, which means they cannot be further divided into parts. These still have properties, for example, we believe that the elementary particles have masses, positions, momenta, spin, and charges.

$^{22}$The arguments of this and the following sections are developed from [17].
When we reach this point we have to ask what methodology we can follow to explain the properties of the elementary particles? As they have no parts, reductionism will not help us. At this point we need a new methodology.

Most thinking about elementary particle physics has taken place in the context of quantum field theory and its descendants such as string theory, which are background dependent theories. Let us start by asking how well these background dependent theories have done resolving the problem of how to attribute properties to particles thought to be elementary. After this we will see if background independent theories can do better.

In a background dependent theory, the properties of the elementary entities have to do with their relationships to the background. This is clear in ordinary quantum field theory, where we understand particles to be representations of the Poincare group and other externally imposed symmetries and gauge invariances. In these theories the particle states are labeled precisely by how they transform under symmetries of the background. The specification of the gauge and symmetry groups are indeed part of the background, because they are fixed for all time, satisfy no dynamical principles and do not evolve.

The search for an explanation of the properties of the elementary particles within quantum field theory and string theory has been based on three hypotheses:

**Unification:** All the forces and particles are different quantum states of some elementary entities.

This elementary entity was at first thought, by Einstein and his friends, to be a field, giving rise to the once maligned subject of unified field theory. In more recent times it is thought to be a string. These are not so far apart, for a low energy approximation to a string theory is a unified field theory. So most actual calculations in string theory involve classical calculations in unified field theories that are descendants of the theories Einstein and friends such as Kaluza and Klein studied many years ago.

But is unification enough of a criteria to pick out the right theory of nature? By itself it cannot be, for there are an infinite number of symmetry algebras which have the observed symmetries as a subalgebra. There is however a second hypothesis which is widely believed.

**Uniqueness:** There exists exactly one consistent unified theory of all the interactions and particles.

If this hope is realized, then it suffices to find that one unified theory. The first fully consistent unified theory to be found will be the only one that can be found and it will thus have to be the true theory of nature. It has even been said that, because of this, physics no longer needs experimental input to progress. At the advent of string theory, this kind of talk was very common. The transition from physics as an experimental science to physics based on finding the single unified theory was even called the passage from modern to
postmodern physics.

Given that, in a background dependent theory, particles are classified by representations of the symmetries of the vacuum, it follows that the more unified a theory is the larger the symmetry of the background must be. This leads to the conjecture of

**Maximal symmetry:** *The unique unified theory will have the largest possible symmetry group consistent with the basic principles of physics, such as quantum theory and relativity.*

These three conjectures have driven much of the work in high energy physics the last three decades. They led first to grand unified theories (large internal gauge groups), then to higher dimensional theories (which have larger symmetry groups) and also to supersymmetry.

While these conjectures come very naturally to anyone with training in elementary particle physics, it must be emphasized that they have arisen from a methodology which is thoroughly background dependent. The idea that the states of a theory are classified by representations of a symmetry group, however used to it we have become, makes no sense apart from a theory in which there is a fixed background, given by the spacetime geometry and the geometry of the spaces in which the fields live. Theories without a background, where the geometry is dynamical and time dependent, such as general relativity, have no symmetry groups which act on the space of their solutions. In general relativity symmetries only arise as accidental symmetries of particular solutions, they have no role in the formulation of the equations or space of solutions of the theory itself.

So the methodology of looking for theories with maximal symmetry only makes sense in a background dependent context. Still, since an enormous amount of work has gone into pursuit of this idea we can ask how far it actually gets us.

The most important thing to know about how this program turned out is that string theories at the background dependent level did not turn out to be unique. There turn out to be five string theories in flat 10 dimensional spacetime background. Each of them becomes an infinite number of theories when the background is taken to be a static but curved spacetime. Many of these are spacetimes in which a certain number of dimensions remain flat while the others are compactified.

To preserve the notion of a unique unification it was conjectured that there is nevertheless a unique unification of all the string theories, which has been called **M** theory. This was motivated by the discovery of evidence for conjectured duality transformations that relate states of the different string theories. This theory, which has so far not been constructed, is conjectured to include all the string theories in 10 dimensions, plus one more theory, which is 11 dimensional supergravity. This is the largest consistent possible supersymmetric gravity theory and, at least at a classical level, naturally incorporates many of the symmetries known or conjectured that act on states of the different string theories.

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23 It must be emphasized that we are talking here of global symmetries, not gauge invariances. Spaces of states or of solutions do not transform under gauge transformations, they are left invariant.
theories.

The search for \( M \) theory has mostly followed the methodology which follows the three principles we mentioned. One posits a maximal symmetry algebra \( A_{\text{max}} \) that contains at least the 11 dimensional super-poincare algebra and then tries to construct a theory based on it. Candidates for this symmetry algebra include the infinite dimensional algebra \( E_{10}[55] \) and compact superalgebras which have the 11 dimensional superpoincare algebra as a subalgebra such as \( Osp(1,32) \) and \( Osp(1,64) \).

However, not much work has been done on the problem of constructing \( M \) theory, despite it being apparently necessary for the completion of the program of unification through symmetry. It is interesting to ask why this is.

If \( M \) theory is to be a unification of all the different background dependent string theories, and hence treat them all on an equal footing, it cannot be formulated in terms of any single spacetime background. Hence, we expect that \( M \) theory must be a background independent theory.

However, background independent theories are very different from background dependent theories, as we have seen already in this essay. One reason for the lack of interest in background independent approaches to \( M \) theory might be simply that is difficult for someone schooled in background dependent methods to make the transition to the study of background independent theories.

But there is a better reason, which is that there is a built in contradiction to the idea of \( M \) theory. As I just emphasized, the idea that \( M \) theory is based on the largest possible symmetry is one that only makes sense in a background dependent context. But as we have also just seen, \( M \) theory must be background independent.

One way out is to posit that the symmetry of \( M \) theory, while acting formally like a background, will not be the symmetry of any classical metric geometry. Indeed this is true of the possibilities studied such as \( E_{11} \) and \( Osp(1,32) \). Still they privilege those geometries whose symmetries are subalgebras of the posited fundamental symmetry, such as the super-poincare algebra. It thus seems hard to avoid a situation in which the solutions which are background spacetimes of maximal symmetry will play a privileged role in the theory. This is unlike the case of general relativity in which the solutions of maximal symmetry may have special properties, like being the ground state with certain asymptotic conditions, but play no special role in the formulation of the dynamics of the theory.

If we are to formulate \( M \) theory as a truly background independent theory, we need a new methodology, tailored to background independent theories. In the next section we will begin a discussion of what a background independent approach to unification might look like.

Before we do, there is one more issue about background dependent theories that we should consider. If the hypothesis of unification is correct, then what accounts for the fact that the observed particles and forces have the particular properties which distinguish them?

The basic strategy of all modern theories of unification is to answer this question with the mechanism of:
**Spontaneous symmetry breaking:** The distinctions between the observed particles and interactions result from a vacuum state of the theory not being invariant under all the symmetries of the dynamics.

This means that the properties that distinguish the different particles and forces from each other are due precisely to their relationship with a choice of background, which is a vacuum state of the theory. If a theory can have different vacuum states, which preserve different subgroups of the symmetries of the dynamics, then the properties of the particles and forces will differ in each. Hence we see explicitly that in these theories the properties of particles are determined by their relationship to the background.

However, notice that something new is happening here, which is quite important for the relational/absolute debate. The point of spontaneous symmetry breaking is that the choice of background is a consequence of the dynamics and can also reflect the history of the system. Hence theories that incorporate spontaneous symmetry breaking take a step in the direction of relational theories in which the properties of elementary particles are determined by their relationships with a dynamically chosen vacuum state.

But if the choice of vacuum state is to be determined dynamically, the fundamental dynamics must be formulated in a way that is independent of a choice of background. That is, the more spontaneous symmetry breaking is used to explain distinctions between particles and interactions, the more the fundamental theory must be background independent.

In conventional quantum field theories this is realized to some extent. But the background of spacetime is generally not part of the dynamics. But in string theory the choice of solution can involve the geometry and topology of space and time. Hence, we arrive again at the necessity to ground string theory on a background independent theory.

### 6.1 The challenge of the string theory landscape

Before we turn to see how to approach the problem of unification from a background independent theory, we should try to draw some lessons from the status of the search based on background dependent methods.

We can begin by asking what tools have string theorists used to study the problem of unification?

A principle tool invoked in much recent work in string theory is effective field theory. An effective field theory is a semiclassical field theory which is constructed to represent the behavior of the excitations of a vacuum state of a more fundamental theory below some specified energy scale. They have the great advantage that one can study a theory expanded around a particular solution, treating that solution as a fixed background. This lets us use many of the intuitions and tools developed in the study of background dependent theories. But there are also disadvantages to the use of effective field theory. One is that the threshold of evidence required to establish as likely a string background is weakened. Whereas it was at first thought necessary to prove perturbative finiteness around
the background to all orders, it is now thought sufficient to display a classical solution to an effective field theory, which is some version of supergravity coupled to branes.

But no effective field theory can stand on its own, for these are not consistent microscopic theories. The reliability of effective field theory must always be justified by an appeal to its derivation from that more fundamental theory. In the applications where it was first developed, effective field theory is derived as an approximation to a more fundamental theory. This is true in $QCD$ and the standard model, as well as in its applications to nuclear physics and condensed matter physics.

We can see this easily by considering cases in which we believe there is no good fundamental theory, such as interacting quantum field theories in 5 or more dimensions. We can construct effective field theories to our heart’s content to describe the low energy physics in such contexts. These may be approximations to cutoff quantum field theories, for example, based on lattices. But they are unlikely to be approximations to any Poincare invariant theories. This is because there is strong evidence that the only Poincare invariant quantum field theories in more than 4 spacetime dimensions are free.

However, in string theory, effective field theory is being used in a context where we do not know that there is a more fundamental theory. That more fundamental theory, if it exists, is the conjectured background independent unification of the different string theories. But since we do not have this theory, either in the form of a set of equations or principles, we cannot be assured that it exists. Hence, by relying on effective field theory we may get ourselves in the situation in which we are studying semiclassical theories which are not approximations to any more fundamental theory.

But, nevertheless, if one insists on confining investigations to background dependent methods, there is little alternative to reliance on effective field theory. In the absence of a derivation from a full quantum theory, one can still posit that the existence of a consistent effective field theory is sufficient to justify belief in a string background, and see where this takes us. One requires a weak form of consistency, which is that excitations of the solution, were they to exist, would be weakly coupled. Not surprisingly, perhaps, this approach leads to evidence for a landscape consisting of an infinite number of discrete string backgrounds[4]. Even restricting the counting to backgrounds that have positive vacuum energy and broken supersymmetry leads to estimates of $10^{500}$ or more discrete vacua[5].

It is interesting to note that the term “landscape” implies the existence of a function, $h$, the height, such that the discrete vacua are at local minima of $h$. In the recent literature, the height $h$ is a potential or free energy. While it is clear what is meant by this, it is perhaps worrying that the concept of energy is problematic in a cosmological or quantum gravity context. This is because, once the gravitational degrees of freedom are included, the energy of cosmological spacetimes is constrained to vanish. All cosmological solutions to diffeomorphism invariant theories have the same energy: zero. There is in cosmology no ground state with zero energy, solutions with different potential energies are no more or less likely to exist, they just expand at different rates. Even if the background geometry is assumed fixed, energy and free energy are only defined on a background that has a
timelike killing field.

But what could the height be, if not energy? The context which inspired the original use of the term landscape in string theory[17], was mathematical models of natural selection, in which the height \( h \) measures the fitness, which is the number of viable progeny of a state. The term was introduced in [17] to evoke the methodologies by which fitness landscapes are studied.

However, in the recent string theory literature on landscapes, the analogy to natural selection is not invoked. What then is the height? If it is energy, then that implies the existence of a fixed background, with a timelike killing field. But what is the background, when the space we are considering is a space of different vacua, with different geometries and topologies? There seems to be a confusion in which reference to a structure that depends on a fixed background is being invoked in the description of the space of possible backgrounds.

Another way to see that the notion of a fixed background is sneaking back into the theory is to consider the assumptions behind the probabilistic studies of the landscape.

There are, broadly speaking, two kinds of methods that might be brought to bear to the study of probability distributions on such landscapes of states. One may study distributions that are in equilibrium, and hence static, or one may study non-equilibrium and hence time dependent distributions.

Almost all the recent work on probability distributions in the string theory landscape have taken the first kind of approach. Some, but not all, of this work evokes what we may call

The anthropic hope: There are a vast number of unified theories, and a vast number of regions of the universe where they may act. Out of all of these, there will be a very small fraction where the laws of physics allow the existence of intelligent life. We find ourselves in one of these. Because the number of universes and theories is so vast, theory can make few prediction except those that follow from requiring our own existence.

The reliance on the anthropic principle is unfortunate, because it can be shown that the use of the anthropic principle cannot lead to any falsifiable predictions. This is argued in detail in [6], to which the reader is referred. As a result, one has to suspect that a search for a unified theory of physics that in the end invokes the anthropic principle has reached a reductio ad absurdum. Somewhere along the line, in the search for a unified string theory, a wrong turn has been taken.

It could be that the wrong turn is that string theory is based on physical hypotheses that have nothing to do with nature. But if this is not the case, some wrong direction must have been taken in the path that led from the conjecture of a unique unification within string theory to the present invocations of the anthropic principle.

We can see from the survey of the situation we just made that the dilemma we have

\[24\text{meaning they will have their own progeny}\]
arrived at seems to involve trying to use background dependent notions, like energy, to do physics in a setting that must be background independent. For if there is a space of possible backgrounds, on which we are to do dynamics, it is obvious that the form of dynamics we employ cannot make reference to any given fixed background. Hence, it seems reasonable to suggest that the wrong turn is the failure to search for a background independent foundation for the theory.

It is then interesting to note that the invocation of static probability distributions harkens back to the absolute perspective. To see this we can ask, what is the time with respect to which the probability distribution is considered to be static? It cannot be the time within a given spacetime background, because the probability distribution lives on the space of possible backgrounds. Single universes may evolve, and may come and go, but there is hypothesized to be nevertheless a static and eternal distribution of universes with different properties. It is this distribution, that exists absolutely and for all time, that we must go for an explanation of any properties of our universe. Thus, at the level of multiverses, static distributions on landscapes have more in common with Aristotle’s way of thinking about cosmology than it does with general relativity.

Is there then an alternative methodology for treating the landscape, which would naturally arise from a background independent theory? I would like to claim there is. The next sections are devoted to its motivation and description.

7 A relational approach to the problems of unification and determination of the standard model parameters

Let us then assume we agree on the need to formulate a unified theory in a background independent framework. Even without having a complete formulation of this kind in hand, it may be of interest to ask what would a background independent approach to the problem of unification look like? How would it address the problems raised in the last section? To approach these questions we return to the question of how we are to explain the properties of the elementary particles?

In a relational theory, as I explained earlier, the properties of the elementary entities can have only to do with relations they have to other elementary entities. Let us explore the implications of this.

The first implication is that any relational system with a large number of parts must be complex, in the sense of having no symmetries. The reason is Leibniz’s principle of the identity of the indiscernible: If two entities have the same relations to the rest, they are to be identified. Each individual entity must then have a unique set of relations to the rest.

The elementary entities in general relativity are the events. An event is characterized by the information coming to it, from the past. We may call the information received by an event in spacetime, the view of that event. It literally consists of what an observer at that event would see looking out their backwards light cone.
It follows that any two events in a spacetime must have different views. This implies that

1. There are no symmetries.
2. The spacetime is not completely in thermal equilibrium.

These are in fact true of our universe. The universe may be homogeneous above the enormous scale of $300 \, Mpc$, but on every smaller scale there is structure. Similarly, while the microwave background is in thermal equilibrium, numerous bodies and regions are out of equilibrium with each other.

Julian Barbour and I call a spacetime in which the view of each event is distinct a Leibniz spacetime. We note, with some wonder, that the fact that our universe is not completely in thermal equilibrium is due to the fact that gravitationally bound systems have negative specific heat, and therefore cannot evolve to unique equilibrium configurations. Furthermore, gravity causes small fluctuations to grow that would otherwise be damped. This is why the universe is filled with galaxies and stars. Thus, gravity, which as Einstein taught us is the force that necessarily exists due to the relational character of space and time, is at the same time the agent that keeps the world out of equilibrium and causes fluctuations to grow rather than to dissipate, which is a necessary condition for it to have a completely relational description.

There is a further consequence of taking the relational view seriously. In a relational theory, the relations that define the properties of elementary entities are not static, they evolve in time according to some law. This means that the properties by which we characterize the interaction of an elementary particle with the rest of the universe are likely to include some which are not fixed a priori by the theory, but depend on solutions to dynamical equations. We can expect that this applies to all of the basic properties that characterize particles such as masses and charges.

8 Relationalism and natural selection

How far can we go to a relational explanation of the properties of the elementary particles in the standard model? While the anthropic principle itself is not explanatory, it is useful to go back to its starting point, which is an apparently true observation, which we may call

**The anthropic observation:** Our universe is much more complex (in for example its astrophysics and chemistry) than most universes with the same laws but different values of the parameters of those laws (including masses, charges, etc.)

This requires explanation. Unfortunately no principle has been found that explains the values of the physical parameters (which can be taken to be the parameters of the stan-
standard models of particle physics and cosmology.) Given recent progress in string theory, there is no reason to expect such a principle to exist. Instead, as the relational argument suggests, those parameters are environmental, and can differ in different solutions of the fundamental theory. We then require a dynamical explanation for the anthropic observation. For it to be science, the explanation must make falsifiable predictions that are testable by real experiments.

There is only one mode of explanation I know of, developed by science, to explain why a system has parameters that lead to much more complexity than typical values of those parameters. This is natural selection.

It may be observed that natural selection is to some extent part of the movement from absolute to relational modes of explanation. There are several reasons to characterize it as such.

- **Natural selection follows the relational strategy.** Before it, properties that characterize species were believed to be eternal, and to have a priori explanations. These are replaced by a characterization of species that is relational and evolves in time as a result of interactions between it and other species.

- **The properties natural selection acts on, such as fitness, are relational quantities, in that they summarize consequences of relations between the properties of a species and other species.**

- **These properties are not fixed in advance, they evolve lawfully.**

- **A relational system requires a dynamical mechanism of individuation, leading to enough complexity that each element can be individuated by its relations to the rest.** Natural selection acts in this way, for example, it inhibits two species from occupying exactly the same niche. By doing so it increases the complexity, measured in terms of the relations between the different species.

This suggests the application of the mode of explanation of natural selection to cosmology.

This has been developed in [17], and it is successful in that it does lead to predictions that are falsifiable, but so far not falsified. The idea, briefly, is the following.

To apply natural selection to a population, there must be:

- A space of parameters for each entity, such as the genes or the phenotypes.

- A mechanism of reproduction.

- A mechanism for those parameters to change, but slightly, from parent to child.

- Differentiation, in that reproductive success strongly depends on the parameters.
By simple statistical reasoning, the population will evolve so that it occupies places in the parameter space leading to atypically large reproductive success, compared to typical parameter values. (Note that creatures with randomly chosen genes are dead.)

This can be applied to cosmology:

- The space of parameters is the space of parameters of the standard models of physics and cosmology. This is the analogue of phenotype. At a deeper level, this is to be explained by a space analogous to genotypes such as the space of possible string theories. This leads to the term the string theory landscape.

- The mechanism of reproduction is the formation of black holes. It is long conjectured that black hole singularities bounce, leading to the formation of new universes through new big bangs. There is increasing evidence that this is true in loop quantum gravity.

- We may conjecture that the low energy parameters do change in such a bounce. There are a few calculations that support this[6].

- The mechanism of differentiation is that universes with different parameters will have different numbers of black holes.

This leads to a simple prediction: our universe has many more black holes than universes with random values of the parameters. This implies that most ways to change the parameters of the standard models of particle physics and cosmology should have fewer black holes.

This leads to testable predictions. I’ll mention one here: there can be no neutron stars with masses larger than 1.6 times the mass of the sun. I will not explain here how this prediction follows, but simply note that it is falsifiable25. So far there all neutron stars observed have masses less than 1.45 solar masses, but new ones are discovered regularly.

9 What about the cosmological constant problem?

It is becoming clearer and clearer that the hardest problem faced by theoretical physics is the problem of accounting for the small value of the cosmological constant problem. The problem is so hard that it constitutes the strongest arguments yet given for an anthropic explanation, following an argument of Weinberg[42] 26

Given that background dependent theories have failed to resolve it, it is important to ask whether background dependent approaches have done any better?

We mention several interesting results here:

25Details of the argument can be found in [17] and[6].
26See [6] for a summary, references and critique.
• There is an argument for the relaxation of the cosmological constant in LQG, analogous to the Pecchi-Quinn mechanism[43]. This relies on a connection between the cosmological constant and parity breaking, which is natural within LQG.

• Volovich has argued, in a particular example, that if spacetime is emergent from more fundamental quantum degrees of freedom, then there is a dynamical mechanism which relaxes the ground state energy[44]. This mechanism is missed if one formulates the theory in terms of an effective field theory that describes only the low energy collective excitations on a fixed background.

• Dreyer argues that the cosmological constant problem is in fact an artifact of background dependent approaches[22]. He proposes that the problem arises from the unphysical splitting of the degrees of freedom of a fundamental, background dependent theory into a background, which has only classical dynamics, and quantum excitations of it. He presents an example from condensed matter physics in which exactly this occurs. In his model, one can calculate the ground state energy two ways: in terms of the fundamental hamiltonian, which is a function of the elementary degrees of freedom, and in terms of an effective low energy hamiltonian which describes collective, emergent low energy degrees of freedom. The zero point energy in the latter overestimates the ground state energy computed in the fundamental theory.

• The only approach to quantum gravity that predicted the correct magnitude of the observed cosmological constant is the causal set theory[45]. There it naturally comes out that a universe with many events has a small cosmological constant. Whether the mechanism that works there extends to other background independent approaches is an interesting open question.

While all these results are preliminary, what is remarkable is that new possibilities for resolving the cosmological constant problem appear when the problem is posed in a background independent theory.

10 The issue of extending quantum theory to cosmology

Let us now turn to the third issue raised in the introduction, whether a cosmological theory can be formulated in the same language as theories of small parts of the universe, or requires a new formulation. As aspect of this is the problem of quantum cosmology. In recent years new proposals to resolve this stubborn problem have been formulated in the context of background independent approaches to quantum gravity.
10.1 Relational approaches to quantum cosmology

In the last ten years several new proposals have been made concerning the foundational issues in quantum cosmology, which have gone under the name of relational quantum theories. These have been inspired by the general philosophy of relationalism.

These approaches have been put forward, in slightly different ways, by Crane, Rovelli and Markopoulou [46, 47, 51]. The mathematical apparatus needed to formalize this view has been studied by Butterfield and Isham [49]. While they differ as to details, they agree that a quantum theory of cosmology is not to be formulated in the language of ordinary quantum mechanics.

One way to state the problem is to ask how we understand the quantum state: Is it a complete and objective description of a physical system, in which case, how do we account for the measurement problem? Or is it a description of the information or knowledge that an observer has about a system they have isolated and studied? If this is the case, can we apply quantum theory to cosmology—or indeed to any system that contains it observers?

There is a hint of relationalism in Bohr, who argued for a view something like the latter. Bohr always insisted that while there must be a line between the system and observer, that line is flexible, it may be drawn anywhere. This is frustrating for those who want to believe in a realist interpretation of the quantum state. A realist would argue that the observer and her instruments are physical systems. Consequently there must be a description in which they are included in the system being studied. Bohr replies there is no contradiction, because now we are speaking of the knowledge a second observer has of a system containing the first observer. According to Bohr then, each observer has a different wavefunction, that describes the system they observe.

Relational approaches to quantum theory formalize this point of view. Rather than taking the Everett/many worlds view, and describing many universe in terms of a single quantum state, they posit that it requires many quantum states to describe a single universe. Each of these quantum states corresponds to a way of dividing the universe into two subsystems, such that one includes an observer.

A relational approach to quantum theory was proposed by Crane [46], in a paper that anticipated some aspects of the holographic principle [48]. In that paper, Crane proposed that there is no quantum state associated with the universe as a whole. Instead, there is a quantum state associated with every way of introducing an imaginary spatial boundary, splitting the universe into two. By analogy with topological field theory, he proposed that the Hilbert spaces on boundaries of 3 + 1 dimensional spacetime should be built up out of state spaces of Chern-Simons theory. When fully developed, this proposal became the very fruitful isolated horizon approach to the quantum geometry and entropy of horizons.

Rovelli then developed a general framework for relational quantum theory [47]. The approaches of Rovelli, however, left open the precise structure that is to tie together the

For references for this section, see the corresponding discussion and references in [7].
network of Hilbert spaces and algebras necessary to describe a whole universe. A template for such structure was given in the work of Butterfield and Isham, who showed how the consistent histories formulation could be interpreted in terms of a sheaf of Hilbert spaces[49].

Markopoulou proposed that the structure tying together the different Hilbert spaces is the causal structure of spacetime[51]. In this formulation there is a Hilbert space for every event in a quantum spacetime. The state at each event is a density matrix that describes the quantum information available to an observer at that event. There are consistency conditions that prescribe how the flow of quantum information in a spacetime follows the causal structure of that spacetime. This is a generalization of quantum theory, for there need not be a quantum state associated with the whole system. (Indeed, it is related to a large class of such generalizations studied by Butterfield and Isham.)

This leads to a relational formulation of the holographic principle, sketched in [52]. The basic idea is that the events are associated with elements of surface. Each corresponds to a quantum channel, by which information flows through from its causal past to its causal future. The area of such a channel is defined to be a measure of its channel capacity.

### 10.2 Relational approaches to going beyond quantum theory

Relational quantum theory gets us out of the paradoxes that arise from trying to describe the universe with a single quantum state. Still, there is, unfortunately, a problem with these approaches. This stems from the fact that the system of quantum states depends on the causal structure of spacetime being fixed. But in a quantum theory of gravity one is supposed to take a quantum sum over all possible histories of the universe, each with a different causal structure. This is to say that relational quantum theories appear to be as background dependent as ordinary quantum theory, it is just that they differ in how they are background dependent.

Can there be a fully background independent approach to quantum theory? I believe that the answer is only if we are willing to go beyond quantum theory, to a hidden variables theory. I would like in closing then to briefly mention work in progress in this direction.

We know from the experimental disproof of the Bell inequalities that any viable hidden variables theory must be non-local. This suggests the possibility that the hidden variables are relational. That is, rather than giving a more detailed description of the state of an electron, relative to a background, the hidden variables may give a description of relations between that electron and the others in the universe.

The possibility of a relational hidden variables theory is suggested by a simple counting argument: In classical mechanics of N point particles, in 3 dimensional space there are $6N$ phase space degrees of freedom. In quantum theory this is described by a complex function on the $3N$ dimensional configuration space-the wavefunction.

But a relational theory has in principle $N^2$ degrees of freedom, at least one for every pair of particles. Most of these are unobservable, by any local observer, because they
involve relations between particles near to us and those very far away. Thus, any working out of a relational theory will have to treat them probabilistically. This will require a probability distribution, which is a real function on $N^2$ variables.

A real function on $N^2$ variables has much more information in it than a complex function on $3N$ variables. Thus, one can imagine deriving quantum mechanics for $3N$ variables from statistical mechanics for $N^2$ variables. Such a theory would be a non-local hidden variables theory.

This leads to a simple conjecture:

Perhaps all the extra information, $N^2$ as compared to $N$, necessary for a completely relational theory, are the non-local hidden variables?

In the last few years two such relational hidden variables theories have been written down. Markopoulou and I have proposed one[53], and Stephen Adler[54], proposes another. In our theory the non-local hidden variables are coded in a graph on $N$ nodes, which is argued to arise from the low energy limit of a relational theory like loop quantum gravity.

It is too soon to see if these theories will be successful. But they offer hope that by taking relational ideas seriously may lead to a successful attack on all five of the problems mentioned in the introduction.

11 Conclusions

In this talk I have described several partly relational, or background independent, theories:

- General relativity
- Relational approaches to quantum gravity, including loop quantum gravity, causal set models, causal dynamical triangulation models and relational approaches to string/$\mathcal{M}$ theory.
- Relational approaches to extending quantum theory to cosmology.

Each is partly successful. Several are more successful than less relational alternatives. But none is completely successful and none is completely relational. They are not completely relational because each still has background structure, which is non-dynamical and must be specified in advance.

However, I believe we do learn something very important from these examples:

In several instances, the relational theory turns out to be more predictive, and more falsifiable than background dependent theories.

In particular, cosmological natural selection leads to falsifiable predictions, which anthropic approaches to the landscape so far do not. Furthermore, there is the very real
possibility that the Planck scale will be probed in upcoming experiments, such as GLAST and AUGER[7]. Background independent theories appear to give predictions for these experiments[41]. String theory cannot, because it takes the symmetry of the background as input.

Why is this the case? I only can make some brief remarks here. The difference between relational and non-relational theories is between:

1) Explanations that refer ultimately to a network of relationships amongst equally physical entities, which evolve dynamically.

2) Explanations that refer to relationships between dynamical entities and an a priori, non-dynamical, background.

The former are more constrained, hence harder to construct. More of what is observed is subject to law, as there is no background to be freely chosen. Hence, it appears that relational, background independent theories are more testable, and more explanatory.

This is the reason for my provocative hypothesis. If it is true that string theory finds itself in the situation described in the introduction is that no background dependent theory could successfully solve the five key problems mentioned there. If this is true, then the only thing to do is to go back and work on the less studied road of relational theories.

At the same time, I have tried here to explain the key problems still faced by the relational road. Some of these have to do with the problem of time. Others have to do with the inverse problem. We saw it in the discussion of causal set models, which are the only purely relational theories I discussed. The inverse problem is that there are many more discrete relational structures than those that approximate local, continuous structures such as classical spacetimes. So a purely relational theory that explains the fact that the world, at least on scales larger than the Planck scale, appears to be continuous and low dimensional, must explain why those local and low dimensional structures dominate in an ensemble of histories most of whom dont remotely resemble local, low dimensional structures.

Let me close by recalling the extent to which the last three decades of theoretical physics are anomalous, compared with the previous history of physics. Many ideas have been studied, but few have been subject to the only kind of test that really matters, which is experiment. The hope behind this paper and the work it represents is that by following the relational strategy we may be led to invent theories that are more falsifiable, whose study will lead us back to the normal practice of science where theory and experiment evolve hand in hand.
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