Cost-Efficient Data Backup for Data Center Networks against $\varepsilon$-Time Early Warning Disaster

Lisheng Ma*, †, Xiaohong Jiang*, Bin Wu‡, Tarik Taleb§, Achille Pattavina¶, and Norio Shiratori∥

*School of Systems Information Science, Future University Hakodate, Hokkaido, 041-8655 Japan
† School of Computer and Information Engineering, Chuzhou University, Chuzhou, 239000 P. R. China
‡ School of Computer Science and Technology, Tianjin University, Tianjin, 300072 P. R. China
§ Department of Communications and Networking, Aalto University, Helsinki, 11000 Finland
¶ Department of Electronics and Information, Politecnico di Milano, Milano, 20133 Italy
∥ GITS, Waseda University, and RIEC, Tohoku University, Japan

Abstract—Data backup in data center networks (DCNs) is critical to minimize the data loss under disaster. This paper considers the cost-efficient data backup for DCNs against a disaster with $\varepsilon$ early warning time. Given geo-distributed DCNs and such a $\varepsilon$-time early warning disaster, we investigate the issue of how to back up the data in DCN nodes under risk to other safe DCN nodes within the $\varepsilon$ early warning time constraint, which is significant because it is an emergency data protection scheme against a predictable disaster and also help DCN operators to build a complete backup scheme, i.e., regular backup and emergency backup. Specifically, an Integer Linear Program (ILP)-based theoretical framework is proposed to identify the optimal selections of backup DCN nodes and data transmission paths, such that the overall data backup cost is minimized. Extensive numerical results are also provided to illustrate the proposed framework for DCN data backup.

Index Terms—Data center networks, cost, data backup, early warning disaster.

I. INTRODUCTION

The rapid growth of communication technology has led to many data-intensive applications that produce huge volumes of data. Most of those applications are relying on data center networks (DCNs) to store and process their huge data. Meanwhile, DCNs are vulnerable to potential disasters. Some recent natural disasters like 2012 Sandy Hurricane, 2011 Japan Tsunami, 2008 China Wenchuan earthquake, etc. [1]–[9], which cause failures of a set of network components and breakdowns of some DCNs. For example, China Wenchuan earthquake in 2008 leads to the damages of over 60 enterprise DCNs [2], [4], and Japan Tsunami and earthquake causes the devastations of tens of DCNs [6], [7]. Thus, in order to improve the survivability of data in DCNs, the data should be backed up among geo-distributed DCNs.

The disasters can be roughly classified into three categories, i.e., predictable disasters, unpredictable disasters, and human made attacks [10], in which predictable disasters (e.g. hurricane, flood, and tsunami) can be forecasted beforehand by atmospheric and environmental conditions. For a predictable disaster, we can obtain an early warning time for DCNs that will be affected by such disaster. Therefore, considering the newly-generated data that fails to be protected by regular backup in those DCNs under risk during the the early warning time, it is highly desirable that such data can be backed up in the other safe DCNs within the early warning time such that the data loss is minimized under disaster.

Given geo-distributed DCNs and a $\varepsilon$-time early warning disaster, for the data hosted at the DCN nodes under risk, we first need to determine the backup DCNs and transmission paths, which will consume time for configuring network. After that data backup can be implemented. Thus, the early warning time should be divided into two parts, i.e., the time for backing up data (referred to as $\varepsilon_1$ hereafter) and that for configuring network (referred to as $\varepsilon_2$ hereafter). To finish the data backup within the early warning time, the tradeoff between backup cost and network resource consumption needs to be taken into account. On one hand, network operators wish to back up data as soon as possible. This can be achieved by consuming huge network resources. On the other hand, data backup involves the costs of storing data in DCNs and data transmission. Thus, a cost-efficient solution is desirable when the time constraint is satisfied.

Regarding data backup in DCNs, the works in [11] and [12] consider the bulk-data transfer in inter-DC networks, which is an essential problem for the data transmission scheduling in DCN data backup. Recently, fast and coordinated data backup in geo-distributed optical inter-DC networks is investigated in [13], in which an ILP is formulated to minimize DC backup window with joint optimization of the backup site selection and the data-transfer paths, and then several heuristics are also proposed. However, this work considers only the mutual backup model and regular backup. Besides, the real-time data replications in DCNs are discussed in [14] and [15], which are different from our work on data backup in DCNs. This because data backup considers to back up huge amount of data that is produced in a period and thus it is not real-time. To the best of our knowledge, no study has been reported for data backup in DCNs against a $\varepsilon$-time early warning disaster.

This paper focuses on data backup in DCNs against a $\varepsilon$-time early warning disaster, in which the data should be backed up in multiple safe DCNs through multiple transmission paths within the early warning time. To have a favorable tradeoff between the backup cost and the network resource consumption, an ILP–based theoretical framework is proposed to identify the
optimal selections of backup DCN nodes and data transmission paths, such that the overall data backup cost is minimized. Our work is significant because it is an emergency data protection scheme against a predictable disaster and also help DCN operators to build a complete backup scheme, i.e., regular backup and emergency backup.

The rest of the paper is organized as follows. Section II introduces the network model and the problem. The ILP for optimal data backup is presented in Section III. We give the numerical results in Section IV and conclude this paper in Section V.

II. NETWORK MODEL AND PROBLEM DESCRIPTION

A. Network Model

We consider the issue of data backup in an optical backbone network. We denote such network as a graph $G(V, E)$, where $V$ is the set of all nodes and $E$ is the set of all fiber links. Each link has a bandwidth capacity which is counted in the number of wavelength channels. The volume of backup data for a specific user is quantified with the number of wavelength channels. The data hosted at the DCNs under risk is transmitted to the backup DCNs through all-optical wavelength channels. The data hosted at the DCNs that are affected by such disaster, we formulate the optimal DCN data backup problem as an ILP problem in Section III.

B. Problem Description

We consider to back up the data in DCNs that are affected by an $\varepsilon$-EWD to other safe DCNs. Our objective is to minimize the total backup cost as detailed in Section II-A with the optimal selections of the backup DCNs and data transmission paths, subject to data in DCNs under risk should be backed up within the $\varepsilon$ early warning time which includes the network configure time and back up time. Given geo-distributed DCNs and a early warning time $\varepsilon$, for the data in the DCNs that affected by such disaster, we formulate the optimal DCN data backup problem as an ILP problem in Section III.

III. ILP FORMULATION

In this section, we first define the notations used in the ILP and then formulate the ILP to optimize the data backup in geo-distributed DCNs against the $\varepsilon$-EWD.

A. Notation List

Inputs:
- $V'$: The set of all safe DCN nodes in network $G(V, E)$.
- $E$: The set of all fiber links in network $G(V, E)$.
- $\varepsilon$: The early warning time for backing up data.
- $P = \{p | p \leftarrow s_p, d_p, L_p >\}$: The set of paths between geo-distributed DCNs where $s_p$ is a DCN node that the data $d$ stored in it and $d_p$ is the amount of the data $d$. $P \in P$ is a set of possible paths for backing up data $d$ where $s_d = s_p$.
- $s_v$: The available storage capacity in DCN node $v \in V'$.
- $B_v$: The available bandwidth capacity on link $e \in E$.
- $W_v$: The cost for a unit amount of data stored in a DCN node $v \in V'$.
- $W_d$: The cost of a wavelength on link $e \in E$.
- $A^p \in \{0, 1\}$: It equals to 1 if link $e \in L_p$.
- $PN$: The maximum allowed number of paths between a pair of DCNs for backing up one user's data.
- $VN$: The maximum allowed number of backup DCNs for backing up one user's data.
- $\lambda$: Predefined constant greater than $max\{B_d^p, N^v_d \mid V \in V', \forall d \in D, \forall p \in P_d\}$.

Variables:
- $M^v_d$: Binary variable. It takes 1 if the DCN node $v \in V'$ is used for backing up data $d \in D$ and 0 otherwise.
- $U^p_d$: Binary variable. It takes 1 if the path $p \in P_d$ is used for backing up data $d \in D$ and 0 otherwise.
- $N^v_d$: Non-negative integer. It is the used storage capacity in node $v \in V'$ for backing up data $d \in D$.
- $B^p_d$: Non-negative integer. It is the used bandwidth capacity on path $p \in P_d$ for backing up data $d \in D$.

B. ILP Formulation

$$\text{Minimize} \left\{ \sum_{d \in D} \left( \sum_{v \in V'} W_v N^v_d + \sum_{p \in P_d} \sum_{e \in L_p} W_e B^p_d \right) \right\}. \quad (1)$$
Subject to

\[ \sum_{d \in D} N_{d}^{v} \leq S_{v}, \forall v \in V; \]  
\[ \sum_{e \in E} A_{d}^{e}B_{d}^{p} \leq B_{e}, \forall e \in E; \]  
\[ \sum_{p \in P_{d}} M_{d}^{v} \geq 1, \forall d \in D; \]  
\[ \sum_{v \in V^{c}} M_{d}^{v} \leq VN, \forall d \in D; \]  
\[ U_{d}^{p} \leq \frac{M_{d}^{p} + 1}{2}, \forall d \in D, \forall p \in P_{d}; \]  
\[ \sum_{p \in P_{d}, D_{p} \neq v} U_{d}^{p} \geq M_{d}^{v}, \forall v \in V^{c}, \forall d \in D; \]  
\[ U_{d}^{p} \leq B_{d}^{p}, \forall d \in D, \forall p \in P_{d}; \]  
\[ U_{d}^{p} \geq B_{d}^{p}/\lambda, \forall d \in D, \forall p \in P_{d}; \]  
\[ M_{d}^{v} \leq N_{d}^{v}, \forall v \in V^{c}, \forall d \in D; \]  
\[ M_{d}^{v} \geq N_{d}^{v}/\lambda, \forall v \in V^{c}, \forall d \in D; \]  
\[ \sum_{p \in P_{d}, D_{p} \neq v} B_{d}^{p} \leq \varepsilon, \forall v \in V^{c}, \forall d \in D. \]  

Objective (1) minimizes the data backup cost, which consists of two terms. The first term is the costs of storing all backup data and the second term is the all bandwidth costs for transmitting the backup data. Constraint (2) ensures that the used storage capacities for backing up data in a safe DCN node do not exceed the available storage capacity of this DCN node. Constraint (3) guarantees that the data for any user can be backed up to the safe DCN nodes. Constraint (4) ensures that the used bandwidth capacities for data backup on a link do not exceed the available capacity of this link. Constraint (5) indicates a bound on the number of paths between the source DCN node (i.e. \(|S_{d}|\)) and a backup DCN node for backing up the data \(d \in D\). Constraint (6) guarantees that any data \(d \in D\) is backed up at least one DCN node while constraint (7) limits the number of backup DCN nodes for the data \(d \in D\) to its maximum possible number. Constraint (8) implies that if a path is selected for backing up the data \(d \in D\), then the destination node of this path must be selected as the backup DCN node for such data. Constraint (9) implies that if a DCN node is selected as the backup node for the data \(d \in D\), then at least one path must be selected as the transmission path for backing up this data in such DCN node. Constraints (10) and (11) define \(U_{d}^{p}\) while constraints (12) and (13) define \(M_{d}^{v}\). Constraint (14) ensures that all data can be backed up in the safe DCN nodes within the \(\varepsilon_{1}\) early warning time for backing up data.

### IV. Numerical Results

In this section, we carry out numerical experiments to validate the proposed ILP. Gurobi 6.0 is used to solve the ILP in (1)-(14). All experiments are run on a computer that has Intel Core(TM) i3-4030U CPU @ 1.90GHz. We consider the DCNs hosted at the U.S. InternetMCI network with 19 nodes and 33 links. We also assume that there is a \(\varepsilon\)-EWD \((\varepsilon = \varepsilon_{1} + \varepsilon_{2})\), which will affect the node 3 location area after \(\varepsilon\) time, as shown by the shaded area in Fig. 2.

The available bandwidth capacity of each link \(B_{e}\) is uniformly distributed within \([10, 20]\) wavelength channels, and the amount of backup data for each user in DCN node 3 is uniformly distributed within \([50, 70]\). We also assume that the total available storage capacity in all safe DCNs is more than the total amount of all backup data, but the available storage capacity in each safe DCN is randomly distributed.

In our experiments, we use the length of link between a pair of nodes as the cost of a wavelength on such link, and then the costs for a wavelength on each link in the U.S. InternetMCI network are shown in Table I. For each backup data and a

| Link | Cost | Link | Cost | Link | Cost |
|------|------|------|------|------|------|
| (0,1) | 625  | (4,8) | 105  | (9,10) | 137  |
| (0,3) | 133  | (4,9) | 240  | (9,16) | 602  |
| (1,2) | 352  | (4,16) | 826  | (11,12) | 393  |
| (2,3) | 488  | (5,8) | 9    | (11,14) | 761  |
| (2,7) | 1309 | (6,7) | 35    | (12,13) | 49   |
| (2,9) | 365  | (6,12) | 223  | (12,14) | 701  |
| (2,10) | 7231 | (7,12) | 249  | (14,15) | 423  |
| (3,7) | 824  | (8,5) | 135  | (14,16) | 532  |
| (3,15) | 209  | (8,14) | 1230 | (15,16) | 128  |
| (3,16) | 256  | (8,16) | 725  | (16,17) | 239  |
| (4,5) | 99   | (8,18) | 500  | (17,18) | 252  |
backup DCN node, $PN$ is set as the number of all possible paths between node 3 and this backup DCN node. We set the cost for a unit amount of data stored in each safe DCN as a random value between 50 and 100. We also set $\lambda = 10000$.

We first consider the data backup cost. In this experiment, the placement of DCNs is illustrated in Fig. 2 where there are four safe DCNs hosted at nodes 9, 12, 14 and 18. All safe DCNs (i.e., DCNs host at nodes 9, 12, 14 and 18) are the candidate backup DCNs for the data from DCN node 3 under risk and $V_N$ is set as 4. For comparison, we also show the data backup approach with the following optimal objective (15) to maximize the overall bandwidth utilization on the paths for data backup (abbreviated as $\text{MaxBandwidthU}$).

$$\text{Maximize } \sum_{d \in D} \sum_{p \in P(d)} B_d^p.$$  

We compare the backup cost between our proposed approach and the MaxBandwidthU approach for different numbers of data $|D|$ (5-20) when $\varepsilon_1 = 70$ seconds, as shown in Fig. 3. We also show the network configure time $\varepsilon_2$ (i.e., computation time for solving ILP) for different numbers of data $|D|$ (5-20) when $\varepsilon_1 = 70$ seconds, as shown in Fig. 4. From Fig. 3, we can find that the data backup costs monotonically decrease with the increase of backup time ($\varepsilon_1$) for our proposed approach. The network configure time that achieved by the MaxBandwidthU approach.

$$\text{Maximize } \sum_{d \in D} \sum_{p \in P(d)} B_d^p.$$  

In Fig. 5, we compare the backup cost for different $\varepsilon_1$ when $|D| = 10$. From Fig. 5, we can find that the data backup costs monotonically decrease with the increase of backup time ($\varepsilon_1$) for our proposed approach. The network configure time
is shown in Fig. 6 for different $\varepsilon_1$ when $|D| = 10$. We can achieve the similar conclusions as those in Fig. 4.

Although the proposed ILP can provide an optimal data backup solution in DCNs for small scale problems against the $\varepsilon$-EWD. However, it will be unavailable for large scale problems (e.g. more candidate backup DCNs, huge amount of backup data and short early warning time) due to the high network configure time (i.e., computation time for solving ILP) which is larger than the early warning time $\varepsilon$. For example, there are 11 DCNs hosted at U.S. InternetMCI network and the data from DCN node 3 under risk should be backed up to other safe DCNs (i.e., safe DCNs host at nodes 2, 5, 7, 8, 9, 11, 12, 14, 15, 16). Here the numbers of data $|D|$ ranges from 5 to 20 and the backup time $\varepsilon_1 = 60$. As illustrated in Fig. 7 we can not obtain an optimal solution within a small scale early warning time (e.g. $\varepsilon$ is less than an hour) when the number of backup data is 20. Thus, the time-efficient heuristic is desirable which is our future work.

V. CONCLUSION

In this paper, we studied the data backup in geo-distributed DCNs against $\varepsilon$-time early warning disaster. For the data hosted at DCN nodes under risk, we consider how to minimize the backup cost with the optimal selections of backup DCN nodes and transmission paths and the early warning time constraint. An ILP-based theoretical framework was proposed to identify the optimal selections of backup DCN nodes and data transmission paths. Numerical results showed that our proposed ILP framework can lead to cost-efficient data backup solution within the early warning time of disaster. Our work is significant because it can help DCN operators to build a complete backup scheme, which includes regular backup and emergency backup. On the other hand, since ILP is not fully scalable for large scale problems, we will develop a time-efficient heuristic to make the data backup problem more scalable.

REFERENCES

[1] K. Tanaka, Y. Yamazaki, T. Okazawa, T. Suzuki, T. Kishimoto, and K. Iwata, “Experiment on seismic disaster characteristics of underground cable.” in The 14th World Conference on Earthquake Engineering, 2008.
[2] “2008sichuan earthquake,” http://en.wikipedia.org/wiki/2008_Sichuan_earthquake
[3] A. Kwasinski, W. W. Weaver, P. L. Chapman, and P. T. Krein, “Telecommunications power plant damage assessment for hurricane katrina-site survey and follow-up results,” IEEE Systems Journal, vol. 3, no. 3, pp. 277–287, Sep. 2009.
[4] Y. Ran, “Considerations and suggestions on improvement of communication network disaster countermeasures after the wenchuan earthquake,” IEEE Communications Magazine, vol. 49, no. 1, pp. 44–47, Jan. 2011.
[5] K. Morrison, “Rapidly recovering from the catastrophic loss of a major telecommunications office,” IEEE Communications Magazine, vol. 49, no. 1, pp. 28–35, Jan. 2011.
[6] “2011tohoku earthquake and tsunami,” http://en.wikipedia.org/wiki/2011_Tohoku_earthquake_and_tsunami
[7] T. Adachi, Y. Ishiyama, Y. Asakura, and K. Nakamura, “The restoration of telecom power damages by the Great East Japan Earthquake,” in IEEE 33rd International Telecommunications Energy Conference, 2011, pp. 1–5.
[8] “Flooding, power outages from hurricane sandy lead to internet, phone service disruptions,” http://www.nypost.com/p/news/business/flooding_from_hurricane_sandy_leads.CG9jI5SStEenIcuZzj1yRbM
[9] A. Kwasinski, “Lessons from field damage assessments about communication networks power supply and infrastructure performance during natural disasters with a focus on hurricane sandy,” in FCC Workshop Network Resiliency, 2013.
[10] B. Mukherjee, M. F. Habib, and F. Dikhinya, “Network adaptability from disaster disruptions and cascading failures,” IEEE Communications Magazine, vol. 52, no. 5, pp. 230–238, May. 2014.
[11] N. Laoutaris, M. Sirivianos, X. Yang, and P. Rodriguez, “Inter-datacenter bulk transfers with netstitcher,” in ACM SIGCOMM, 2011, pp. 74–85.
[12] A. Mahimkar, A. Chiu, R. Doervespike, M. Feuer, P. Magill, E. Mavrogjorgis, J. Pastor, S. Woodward, and J. Yates, “Bandwidth on demand for inter-data center communication,” in ACM HotNets, 2011, pp. 24–29.
[13] J. J. Yao, P. Lu, L. Gong, and Z. Q. Zhu, “On fast and coordinated data backup in geo-distributed optical inter-datacenter networks,” IEEE/OSA Journal of Lightwave Technology, vol. 33, no. 14, pp. 3005–3015, Jul. 2015.
[14] D. Boru, D. Kliazovich, F. Granelli, P. Bouvry, and A. Zomaya, “Energy-efficient data replication in cloud computing datacenters,” Cluster Computer, vol. 18, pp. 385–402, Jan. 2015.
[15] R. S. Couto, S. Secci, M. E. M. Campista, and L. H. M. Costa, “Server placement with shared backups for disaster-resilient clouds,” Computer Networks, vol. 93, pp. 423–434, Dec. 2015.
[16] “InternetMCI network,” http://www.topology-zoo.org/dataset.html, 2011.