Spiking Neural Networks –
Part III: Neuromorphic Communications
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Abstract—Synergies between wireless communications and artificial intelligence are increasingly motivating research at the intersection of the two fields. On the one hand, the presence of more and more wirelessly connected devices, each with its own data, is driving efforts to export advances in machine learning (ML) from high performance computing facilities, where information is stored and processed in a single location, to distributed, privacy-minded, processing at the end user. On the other hand, ML can address algorithm and model deficits in the optimization of communication protocols. However, implementing ML models for learning and inference on battery-powered devices that are connected via bandwidth-constrained channels remains challenging. This paper explores two ways in which Spiking Neural Networks (SNNs) can help address these open problems. First, we discuss federated learning for the distributed training of SNNs, and then describe the integration of neuromorphic sensing, SNNs, and impulse radio technologies for low-power remote inference.

I. INTRODUCTION

Machine Learning (ML) and wireless communications are increasingly seen as mutually beneficial, with each technology motivating advances and new applications for the other. On the one end, current advances in ML have been largely fueled by a wider availability of data and by an increase in computing power available on large centralized mixed CPU-GPU clusters. This learning approach, with its reliance on massive amounts of data and computing power, raises accessibility, sustainability, and privacy concerns [1]. These concerns may be addressed by migrating some of the ML applications to a learning paradigm empowered by wireless among mobile devices. This emerging framework, termed Federated Learning (FL) [2], [3], enables collaborative inter-device training without direct exchange of data.

On the other hand, novel wireless communication applications, including the deployment of Internet of Things (IoT) networks, pose new problems that challenge the conventional design paradigm that keeps the optimization of sensing, computing, and communication separate. To use spectral resources more effectively, a recently emerging line of research [4]–[8] focuses on applying ML to train a communication system in an end-to-end fashion by targeting directly application-level performance criteria. Notable examples include [8], in which compression and transmission are jointly optimized to minimize the distortion in the transmission of images over wireless links.

As discussed also in Part I and II of this three-part paper [9], [10], model architectures that implement standard Artificial Neural Networks (ANNs) may not be the best choice to meet the energy limitations in battery-powered devices. In contrast, Spiking Neural Networks (SNNs) have recently emerged as a low-power alternative thanks to their ability to process information in an event-driven, sparse, and online fashion. SNNs also offer strong synergies with neuromorphic sensors that record spiking signals, e.g., from neural prosthetics or silicon retinas, and with impulse radio (IR) communication systems that encode information using the timing of radio pulses [11]–[13]. IR is a technology of choice for low-power communications. It has been specified by the IEEE 802.15.4z standard, and is investigated for beyond-5G terahertz communication systems [14].

In this paper, we review two applications of SNNs for communication systems. In Sec. [4] as illustrated in Fig. [1] we describe an implementation of joint learning via FL that trains on-device SNNs following reference [15]. We discuss some of the novel performance trade-offs that arise when training SNNs instead of ANNs. Then, in Sec. [3] as seen in Fig. [2] we discuss an end-to-end neuromorphic system, for which recording, processing, transmission, and classification are carried out using spiking signals by integrating neuromorphic sensors, SNNs, and IR as in [16]. We demonstrate significant advantages in terms of time to accuracy and energy efficiency over standard frame-based and digital schemes.
Fig. 2: End-to-end neuromorphic sensing, processing, and communications based on spiking sensors, SNNs, and impulse radio (IR).

II. COMMUNICATIONS FOR NEUROMORPHIC LEARNING: FL-SNN

A. Overview

FL has recently emerged as the standard term to describe distributed learning protocols based on the exchange of model, rather than data, information with the aim of exploring low-power implementations for on-device training. Unlike standard implementations based on ANNs, we consider the joint training of on-device SNNs via FL.

The system, referred to as FL-SNN, consists of $N$ devices communicating through a base station (BS). Each device $d = 1, \ldots, D$ holds a different local data set $D^{(d)}$ that contains a collection of $|D^{(d)}|$ data points. Following the notation introduced in Part II ([10]), each data point is given by a target spiking signals $x_{\leq T}^{(d)}$ of duration $T$ samples. The goal of FL is to train a common model based on the global dataset $D = \bigcup_{d=1}^{N} D^{(d)}$ without direct exchange of the data from the local data sets. The training objective of FL-SNN is to solve the problem

$$
\min_{\theta} F(\theta) := \frac{1}{\sum_{d=1}^{N} |D^{(d)}|} \sum_{d=1}^{D} |D^{(d)}| F^{(d)}(\theta),
$$

where $F(\theta)$ is the global empirical loss over the global data set $D$; and the local empirical loss at a device $d$ is defined as

$$
F^{(d)}(\theta) = \frac{1}{|D^{(d)}|} \sum_{x_{\leq T}^{(d)} \in D^{(d)}} f(\theta, x_{\leq T}^{(d)}),
$$

where $f(\theta, x_{\leq T}^{(d)})$ is the loss function measured on target $x_{\leq T}^{(d)}$ under model parameter vector $\theta$.

Throughout this paper, we adopt the GLM-based SNN model. Referring to [15] for details, we denote as $x_{\leq T}^{(d)}$ the set of visible neurons in the read-out layer, and as $H^{(d)}$ the rest of the neurons in the SNN of device $d$, which are also known as hidden neurons. Each neuron $i$ keeps track of membrane potential variable $u_{i,t}^{(d)}$ that evolves as a function of the spikes produced by pre-synaptic neurons through the synaptic weights $\{w_{i,k}^{(d)}\}$, where $k$ is the index of a pre-synaptic neuron. The spiking probability for neuron $i$ at device $d$ conditioned on the previous outputs of all neurons is given as

$$
p_{\theta_{i}^{(d)}}(s_{i,t}^{(d)}) = 1[u_{i,t}^{(d)}] = \sigma(u_{i,t}^{(d)}),
$$

where $\sigma(a) = 1 + \exp(-a)$ is the sigmoid function and $\theta_{i}^{(d)}$ is the vector of model parameters for neuron $i$. By (3), the negative log-probability of the spike is given as $-\log p_{\theta_{i}^{(d)}}(s_{i,t}^{(d)}|u_{i,t}^{(d)}) = \ell_{i}(s_{i,t}^{(d)}, \sigma(u_{i,t}^{(d)})),$ where $\ell(a, b) = -a \log(b) - (1-a) \log(1-b)$ is the binary cross-entropy loss function.

Accordingly, the loss function $f(\theta, x_{\leq T}^{(d)})$ is chosen as the log-loss $f(\theta, x_{\leq T}^{(d)}) = -\log p_{\theta}(x_{\leq T}^{(d)})$, where $p_{\theta}(x_{\leq T}^{(d)}) = \prod_{t=1}^{T} \prod_{i \in x_{\leq T}^{(d)}} p_{\theta_{i}^{(d)}}(x_{i,t}^{(d)}|u_{i,t}^{(d)}) = \prod_{t=1}^{T} \prod_{i \in x_{\leq T}^{(d)}} \sigma(u_{i,t}^{(d)})$ is the probability that the read-out layer of visible neurons $x_{\leq T}^{(d)}$ outputs the target signal $x_{\leq T}^{(d)} \in D^{(d)}$. The computation of the training loss function requires to average out the stochastic signals $h_{\leq T}^{(d)}$ produced by the hidden neurons $H^{(d)}$, which is generally intractable. Using the causally conditioning notation [17] introduced in Part II [10] and Jensen’s inequality, the log-loss is upper bounded as

$$
f(\theta, x_{\leq T}^{(d)}) = -\log \mathbb{E}_{p_{\theta}(h_{\leq T}^{(d)}|x_{\leq T}^{(d)})} [p_{\theta}(x_{\leq T}^{(d)}|h_{\leq T}^{(d)})] 
\leq \mathbb{E}_{p_{\theta}(h_{\leq T}^{(d)}|x_{\leq T}^{(d)})} \left[ \sum_{t=1}^{T} \sum_{i \in x_{\leq T}^{(d)}} \ell_{i}(x_{i,t}^{(d)}, \sigma(u_{i,t}^{(d)})) \right].
$$

The key advantage of bound (4) is that it decomposes over the time index $t$. In FL, training is carried iteratively at each device $d$ via gradient descent updates and periodic averaging of the model parameters across devices. The local updates are computed at each local iteration $j = 1, \ldots, J$. In FL-SNN, these iterations are embedded into the finer-grained time scales $t = 1, 2, \ldots$ at which spikes are processed by the on-device SNNs. Specifically, each local iteration $j$ is applied every $\Delta t \geq 1$ SNN time steps, that is at the end of the interval $[j] = \{ t: (j-1)\Delta t + 1 \leq t \leq j \Delta t \}$. The total number of SNN time-steps and the number $J$ of local iterations are hence related as $N \cdot T = J \Delta t$, where $N$ is the number of training examples presented sequentially in an online fashion. Note that Part II of this review presented the local updates for the special case where $\Delta t = 1$ (Sec. III.B), and we detail below how to generalize the training rule to $\Delta t > 1$.

Every $\Delta J$ local iterations, each device $d$ uploads its current model iterate $\theta_{i}^{(d)}$ to the BS, which computes the centralized averaged parameter

$$
\theta = \frac{1}{\sum_{d=1}^{D} |D^{(d)}|} \sum_{d=1}^{D} |D^{(d)}| \theta_{i}^{(d)},
$$

before sending it back to all devices via multicast downlink transmission. Each device $d$ then initializes its local parameter to $\theta$ for the local updates in iteration $j + 1$.

Local updates of $\theta_{i}^{(d)}$ are performed at the SNN of each device $d$ by optimizing via gradient descent an upper bound on the local loss (4). The rule follows the online gradient steps described in Part II, applied every $\Delta t$ time steps. Specifically, the $j$-th local update rule for the synaptic weight $w_{i,k}^{(d)}$ between
pre-synaptic neuron $k$ and post-synaptic neuron $i$ in the SNN of device $d$ is given as

$$\Delta w^{(d)}_{i,k}(j) = \sum_{t \in [j]} \left( x_{i,t}^{(d)} - \sigma\left( u_{i,t}^{(d)} \right) \right) (\alpha_t * s^{(d)}_{k,t}), \quad \text{for } i \in \mathcal{X}^{(d)},$$

$$\sum_{t \in [j]} \epsilon_{i,t}^{(d)} \left( h_{i,t}^{(d)} - \sigma\left( u_{i,t}^{(d)} \right) \right) (\alpha_t * s^{(d)}_{k,t}), \quad \text{for } i \in \mathcal{H}^{(d)},$$

where we set $s^{(d)}_{i,t} = x_{i,t}^{(d)}$ as the target spiking signal at time $t$ for any visible neuron $i \in \mathcal{X}^{(d)}$; we use the notation $s^{(d)}_{i,t} = h_{i,t}^{(d)}$ for the binary output of any hidden neuron $i \in \mathcal{H}^{(d)}$ at time $t$; $\alpha_t$ is the filter representing the synaptic spike response; $*$ is the convolution operator; and the global error signal $\epsilon_{i,t}^{(d)}$ at device $d$ is computed as

$$\epsilon_{i,t}^{(d)} = \sum_{t \in [j]} \ell(x_{i,t}^{(d)}, \sigma(u_{i,t}^{(d)})).$$

The resulting algorithm is summarized in [15].

B. Experiments

We consider the task of classifying handwritten digits displayed to a neuromorphic camera, which were recorded as part of the MNIST-DVS dataset [18]. We follow the preprocessing procedure detailed in [15], which yields 676 input spiking signals with $T = 80$ time-steps from images of size $26 \times 26$.

Digits are split across $D = 2$ devices, with the first device having access only to examples of digit “1”, and the second having access only to examples from digit “7”. Neurons in both on-device SNNs are densely connected, and exogenous inputs are connected to all neurons.

In Fig. 3, we highlight the impact of the choice of the number $\Delta t$ of time-steps between local updates and of the number $\Delta J$ of local updates between communication rounds. Note that the number of time-steps between communication rounds is $\Delta t \times \Delta J$. The top figure is obtained with $\Delta t = 1$, and the bottom figure with $\Delta t = 10$. We report test accuracy with different values of $\Delta J$ during training from a random initialization, averaged over both devices and three repetitions of the experiment.

With $\Delta t = 1$, local updates have a higher variance, but they are more frequent. More frequent local updates also enable a larger number of communication rounds for a given number of time-steps. With $\Delta t = 10$, updates are averaged over ten time-steps, and are hence less noisy, but occur less often. Fig. 3 shows that the best performance is obtained with $\Delta t = 10$, which ensures lower-variance updates, and $\Delta J = 1$, which yields frequent communication rounds. Note that, with $\Delta t = 1$ and $\Delta J = 1$, training is initially slow since the first communication rounds are impaired by the noisy local updates. Furthermore, when $\Delta t = 10$ and $\Delta J = 8$ or 80, communication is too infrequent to allow for collaborative training and the test accuracy is limited by overfitting on the local data. As a result, after the improvement caused by a communication round, the performance quickly drops back to yield a classifier with worst-case performance. We refer to [15] for a study of the trade-offs in the case of a limited communication budget.

III. NEUROMORPHIC LEARNING FOR COMMUNICATIONS: NEUROJSCC

A. Overview

In this section, we describe a system that processes information, from sensing to inference, in the form of sparse, spiking signals, by integrating neuromorphic sensors, SNNs, and IR. Data is recorded using a neuromorphic low-power sensor, and inference is performed at a remote battery-powered device to which the sensor is wirelessly connected through a low-power radio interface.

As seen in Fig. 2, physical signals are recorded using a neuromorphic sensor, and encoded as a vector $o_{\leq T}$ of $d_o$ spiking signals across $T$ time-steps. For example, the recorded data may be obtained from a DVS camera [19], to which an object or an activity belonging to a certain class is displayed. The sensed signals are fed as inputs to an encoding SNN that outputs $d_e$ spiking signals $x_{\leq T}$. We denote as $\mathcal{X}$ the set of (hidden) output neurons, and as $\mathcal{H}^E$ the rest of the hidden neurons in the encoding SNN. We denote the probabilistic mapping of the encoding SNN as $p_{\theta^E}(x_{\leq T}|o_{\leq T}) = \prod_{t=1}^T p(x_{\leq t}|x_{\leq t-1}, o_{\leq t})$, where superscript $E$ denotes the encoder. The encoded signals $x_{\leq T}$ are modulated by using $d_e$ parallel IR transmissions, with each spike encoded by an IR waveform such as a Gaussian monopulse.

The channel output $y_{\leq T}$ at time $t$ is generally stochastic and depends on its past inputs $x_{\leq t-1}$ up to time $t - 1$. It includes the effect of waveform generation at the transmitter, intersymbol interference, as well as filtering and thresholding at the receiver. As a result, we assume that the received signal $y_{\leq T}$ is binary. The channel can be expressed as the causally conditional distribution $p(y_{\leq T}|x_{\leq T})$.

The received signals $y_{\leq T}$ are fed to a decoding SNN that produces $d_o$ output spiking signals $v_{\leq T}$, via a probabilistic mapping $p_{\theta^D}(v_{\leq T}|y_{\leq T})$ with a learnable parameter vector $\theta^D$. The decoding SNN comprises the set $\mathcal{V}$ of visible output neurons in the read-out layer and the set $\mathcal{H}_o^D$ of hidden
neurons. The output of the decoding SNN \( v_{\leq T} \) is used for inference, e.g., to predict a class index using standard methods for SNN-based classification [20, 21], such as rate encoding described in Part II.

A data set of input-output pairs \((o_{\leq T}, v_{\leq T})\), is available for training. Combining all elements, the joint distribution \( p_\theta(o_{\leq T}, v_{\leq T}) \) of the end-to-end system is parameterized by encoder and decoder parameters as \( \theta = \{ \theta^E, \theta^D \} \).

**B. NeuroJSCC**

The task of jointly implementing compression and error-correcting codes is known in the literature as Joint Source-Channel Coding (JSCC). In the system outlined above, JSCC is implemented by using the encoding and decoding SNNs. We hence refer to this solution as *NeuroJSCC*. The end-to-end optimization of the system is carried out by maximizing the log-likelihood of the decoding SNN outputs desired spiking signals \( v_{\leq T} \) in response to a given input \( o_{\leq T} \). Mathematically, in a manner similar to FL-SNN, NeuroJSCC tackles the problem of minimizing the training log-loss [20] over a training set \( D \).

The log-loss \(- \log p_\theta(v_{\leq T} | o_{\leq T})\) in \([9]\) is obtained by averaging over the distribution \( p_\theta(h^E_{\leq T}, x_{\leq T}, y_{\leq T}, h^D_{\leq T} | v_{\leq T}, o_{\leq T})\) of signals \( h^E_{\leq T} \) and \( h^D_{\leq T} \) produced by the hidden neurons of encoder and decoder, as well as the channel’s inputs and outputs \( x_{\leq T} \) and \( y_{\leq T} \) as

\[
\log p_\theta(v_{\leq T} | o_{\leq T}) = \log \mathbb{E}_{p_\theta}
\left[
\langle h^E_{\leq T}, x_{\leq T}, y_{\leq T}, h^D_{\leq T} | v_{\leq T}, o_{\leq T} \rangle
\right].
\]

To address problem \((8)\), as in the derivation of the learning rule \([9]-[7]\), we apply stochastic gradient descent on the upper bound obtained via Jensen’s inequality (see Part II and [16] for details)

\[
- \log p_\theta(v_{\leq T} | o_{\leq T}) \leq \mathbb{E}_{p_\theta}(h^E_{\leq T}, x_{\leq T}, y_{\leq T}, h^D_{\leq T} | v_{\leq T}, o_{\leq T}) \left[ \sum_{t=1}^{T} \sum_{i \in \mathcal{V}} \ell(v_{i, t}, \sigma(x_{i, t})) \right].
\]

As in \([9]-[7]\), gradients are approximated via Monte Carlo estimates by drawing samples \( h^E_{\leq T}, x_{\leq T}, y_{\leq T}, h^D_{\leq T} \) of the hidden neurons and channel outputs via the forward operation of the system described by distribution \( p_\theta(h^E_{\leq T}, x_{\leq T}, y_{\leq T}, h^D_{\leq T} | v_{\leq T}, o_{\leq T}) \), yielding the update

\[
\Delta \theta_{i,k} = \begin{cases} 
(\sigma(v_{i, t}) - \sigma(u_{i, t})) & \text{for } i \in \mathcal{V}, \\
\ell_i(s_{i, t} - \sigma(u_{i, t})) & \text{for } i \in \mathcal{H}^E, \mathcal{X}, \mathcal{H}^D,
\end{cases}
\]

where \( v_{i, t} \) is the target spiking signal at time \( t \) for any visible neuron \( i \in \mathcal{V} \); \( s_{i, t} \) denotes the binary output of any hidden neuron \( i \in \mathcal{H}^E, \mathcal{X}, \mathcal{H}^D \) at time \( t \); and the global error signal is computed as

\[
\tilde{e}_t = \sum_{i \in \mathcal{V}} \ell(v_{i, t}, \sigma(x_{i, t})).
\]

The resulting algorithm is detailed in [16].

**C. Experiments**

In this section, we consider again the problem of classifying between examples of digits “1” and “7” from the MNIST-DVS dataset. We introduce the communication rate \( r = \frac{d_x}{d_y} \) as the ratio between the number of transmitted and input signals at each time-step. We transmit signals through a Gaussian channel, for which we adjust the noise power \( \sigma^2 \) in order to ensure the same SNR level for all schemes. We define the per-symbol transmission signal-to-noise (SNR) ratio as \((\frac{\|x_{\leq T}\|_1}{(d_x d_y)})/\sigma^2\). To obtain binary inputs at the receiver side, the noisy samples are quantized with a hard threshold at 0.5. The system of interest is comprised of an encoding SNN with no hidden neurons, and for which all of the 676 exogeneous inputs are connected to the \( d_x = r d_y \) neurons in the output layer. The decoding SNN presents a fully connected architecture with \( d_y = d_x \) exogeneous inputs, \( N^H = d_x \) internal neurons, and \( d_v = 2 \) output neurons – one for each class.

As in [16], we compare NeuroJSCC to two schemes. With *Uncoded transmission*, samples are directly transmitted through the channel using On-Off Shift Keying (OOK), yielding a rate \( r = 1 \). The received are classified using a GLM-based SNN as described in Part II with \( N^H = 256 \) hidden neurons. The second benchmark system is a frame-based *Separate Source-Channel Coding (SSCC)*, which uses state-of-the-art quantization with Vector-Quantization Variational Autoencoder (VQ-VAE) [22], and LDPC encoding. The rates of source and channel encoders are chosen to obtain \( r = 1 \). The scheme divides the input samples into \( F \) frames of size \([T/F]\). Frames are classified at the receiver side using either
obtain privacy-minded and energy-efficient distributed learning in synergy with wireless communication systems. On the one hand, SNNs can be integrated with federated learning (FL) to ensure low-energy and low-latency remote inference. These solutions exemplify the realm of possibilities offered by the intersection of neuromorphic computing and communications.

IV. CONCLUSIONS

In this paper, the last of a three-part review on SNNs [9], [10], we have discussed how SNNs can beneficially be used in synergy with wireless communication systems. On the one hand, SNNs can be integrated with federated learning (FL) to obtain privacy-minded and energy-efficient distributed learning solutions. We have demonstrated by experiments benefits over separate training. On the other hand, neuromorphic sensing and computing can be integrated with impulse radio (IR)-based transmission to ensure low-energy and low-latency remote inference. These solutions exemplify the realm of possibilities offered by the intersection of neuromorphic computing and communications.

REFERENCES

[1] E. Strubell, A. Ganesh, and A. McCallum, “Energy and policy considerations for deep learning in NLP,” arXiv preprint arXiv:1906.02243, 2019.
[2] S. Wang et al., “Adaptive federated learning in resource constrained edge computing systems,” IEEE Journal on Selected Areas in Communications, vol. 37, no. 6, pp. 1205–1221, 2019.
[3] H. McMahan, E. Moore, D. Ramage, S. Hampson, and B. Agarwal, “Communication-efficient learning of deep networks from decentralized data,” in Proc. of International Conference on Artificial Intelligence and Statistics, 2017.
[4] T. O’Shea and J. Hoydis, “An introduction to deep learning for the physical layer,” IEEE Transactions on Cognitive Communications and Networking, vol. 3, no. 4, pp. 563–575, 2017.
[5] O. Simeone, “A brief introduction to machine learning for engineers,” Foundations and Trends® in Signal Processing, vol. 12, no. 3-4, pp. 200–431, 2018.
[6] K. Choi, K. Tatwawadi, A. Grover, T. Weissman, and S. Ermon, “Neural joint source-channel coding,” in Proc. of International Conference on Machine Learning, 2019.
[7] V. Raj and S. Kalyani, “Design of communication systems using deep learning: A variational inference perspective,” IEEE Transactions on Cognitive Communications and Networking, 2020.
[8] E. Bourtsoulatze, D. Barth Karka, and D. Gündüz, “Deep joint source-channel coding for wireless image transmission,” IEEE Transactions on Cognitive Communications and Networking, vol. 5, no. 3, pp. 567–579, 2019.
[9] H. Jang, N. Skatchkovsky, and O. Simeone, “Spiking neural networks – Part I: Detecting spatial patterns,” submitted.
[10] N. Skatchkovsky, H. Jang, and O. Simeone, “Spiking neural networks – Part II: Detecting spatio-temporal patterns,” submitted.
[11] A. Cassidy, Z. Zhang, and A. G. Andreou, “Impulse radio address event interconnects for body area networks and neural prostheses,” in Proc. of Argentine School of Micro-Nanoelectronics, Technology and Applications, IEEE, 2008.
[12] A. Shahshahani et al., “An all-digital spike-based ultra-low-power IR-UWB dynamic average threshold crossing scheme for muscle force wireless transmission,” in Proc. of Design, Automation & Test in Europe Conference & Exhibition. IEEE, 2015.
[13] F. Peper, K. Leibnitz, J.-n. Teramae, T. Shimokawa, and N. Wakamiya, “Low-complexity nanosensor networking through spike-encoded signaling,” IEEE Internet of Things Journal, vol. 3, no. 1, pp. 49–58, 2015.
[14] X. Yu, M. Galli, T. Morioka, P. U. Jepsen, and L. K. Oxenløwe, “Towards ultrahigh speed impulse radio THz wireless communications,” in Proc. of International Conference on Transparent Optical Networks. IEEE, 2015.
[15] N. Skatchkovsky, H. Jang, and O. Simeone, “Federated neuromorphic learning of spiking neural networks for low-power edge intelligence,” in Proc. of International Conference on Acoustics, Speech and Signal Processing. IEEE, 2020.
[16] N. Skatchkovsky, H. Jang, and O. Simeone, “End-to-end learning of neuromorphic wireless systems for low-power edge artificial intelligence,” arXiv preprint arXiv:2009.01527, 2020.
[17] G. Kramer, Directed information for channels with feedback. Hartung-Gorre, 1998.
[18] T. Serrano-Gotarredona and B. Linares-Barranco, “Poker-DVS and MNIST-DVS: Their history, how they were made, and other details,” Frontiers in Neuroscience, vol. 9, p. 481, 2015.
[19] P. Lichtsteiner, C. Posch, and T. Delbruck, “A 128 × 128 120dB 30mW asynchronous vision sensor that responds to relative intensity change,” in Proc. of International Solid-State Circuits Conference. IEEE, 2006.
[20] H. Jang, O. Simeone, B. Gardner, and A. Grünig, “An introduction to probabilistic spiking neural networks: Probabilistic models, learning rules, and applications,” IEEE Signal Processing Magazine, vol. 36, no. 6, pp. 64–77, 2019.
[21] A. Stanojevic, G. Cherubini, T. Moraitis, and A. Sebastian, “File classification based on spiking neural networks,” arXiv preprint arXiv:2004.03953, 2020.
[22] A. Van Den Oord, O. Vinyals et al., “Neural discrete representation learning,” in Proc. of Advances in Neural Information Processing Systems, 2017.
[23] L. Deng et al., “Rethinking the performance comparison between snn and anns,” Neural Networks, vol. 121, pp. 294–307, 2020.