Disorder strength measured by quantitative phase imaging as intrinsic cancer marker in fixed tissue biopsies

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Abstract

Tissue refractive index provides important information about morphology at the nanoscale. Since the malignant transformation involves both intra- and inter-cellular changes in the refractive index map, the tissue disorder measurement can be used to extract important diagnosis information. Quantitative phase imaging (QPI) provides a practical means of extracting this information as it maps the optical path-length difference (OPD) across a tissue sample with sub-wavelength sensitivity. In this work, we employ QPI to compare the tissue disorder strength between benign and malignant breast tissue histology samples. Our results show that disease progression is marked by a significant increase in the disorder strength. Since our imaging system can be added as an upgrading module to an existing microscope, we anticipate that it can be integrated easily in the pathology work flow.

Introduction

Breast cancer is the most commonly diagnosed type of cancer among women worldwide [1]. Furthermore, according to the American Cancer Society, the incidence of breast cancer in the US is on the rise, with 200,000 new cases expected in the year 2017 [2]. While the burden of disease is significant, standard breast histopathology still relies on manual microscopic inspection of Hematoxylin and Eosin (H&E) stained tissue. The H&E primary stain provides the necessary contrast needed for a trained pathologist to distinguish between normal and abnormal tissue morphology. However, this type of investigation is qualitative, depends on the details of tissue processing and, as a result, often leads to inter-observer variability. Thus, there is a need to provide an objective basis for evaluation based on physical metrics. For cases where information provided by the H&E stain is limited and diagnosis is difficult, specialized stains can help pathologists [3]. New quantitative markers can provide objective assessment, as well as information complementary to traditional biomarkers. Specific information on tumor cell
biology, extracted by such intrinsic markers, can also potentially lead to automated computer algorithms.

Quantitative phase imaging (QPI) is a label-free microscopy technique where contrast is generated by the optical path-length difference (OPD) across a tissue specimen [4–7]. The phase image $\phi(x,y)$ extracted in QPI is given by the expression

$$\phi(x,y) = \frac{2\pi}{\lambda} n(x,y)L(x,y),$$

where $n(x,y)$ is the refractive index contrast between the tissue and the surrounding medium (mounting medium in the case of histology samples), $L(x,y)$ is the tissue thickness and $\lambda$ the illumination wavelength [4]. For precise histological sections, the tissue thickness can be assumed to be relatively constant, $L(x,y) \approx L$, meaning that a QPI measurement provides a signal that is proportional to the refractive index map of tissue. Since it is proportional to the dry mass content of cells and cellular matrix, the refractive index map informs on tissue density as well as cell organization within tissue [8, 9]. Since QPI allows extraction of the refractive index map label-free, the extracted biological markers are intrinsic, meaning that the results are not susceptible to variation due to differing staining procedures, thus, providing a robust signal for automated analysis. Tissue refractive index based markers have been used in the past to separate benign and malignant prostate tissue [10] as well as for detection of pre-malignancy in colorectal tissue [11]. OPD maps in general, extracted using QPI, have been used for addressing quantitative histopathology problems in prostate, colon, breast, pancreatic and other cancers etc. [12–20].

The tissue metric referred to as “disorder strength” was first used for diagnosis by Subramanian et al. [21]. The authors used it as a means of probing the sub-wavelength spatial fluctuations of refractive index and, thus, to detect carcinogenesis undetectable by standard histopathology [22–31]. Since QPI systems employ interferometric measurements, they are sensitive to sub-wavelength fluctuations in the refractive index map in both space and time [4]. Eldridge et al. measured the disorder strength using QPI and demonstrated that a transformation in cell mechanical properties can be measured by quantifying the cell disorder strength [32]. They applied this analysis to colon, skin and lung cancer cells to demonstrate an inverse relationship between sheer stiffness and disorder strength [32]. Furthermore, A. Muñoz et al. evaluated the shear stiffness of populations of cells during transformation to a carcinogenic state using a QPI-based method and applied it to identify the development of cancerous cells [33].

Here, we propose to use the disorder strength as an intrinsic marker for classifying benign and malignant breast tissue. We imaged a tissue microarray (TMA) comprising of cores obtained from cancer and normal-control patients. Details of this sample can be found in [13]. Each core was diagnosed as either benign or malignant by a board certified pathologist by examining H&E stained tissue images of a parallel tissue section. From this TMA, we studied 20 benign cores and 20 malignant cores. Since malignancy causes changes in both tissue architecture at the nanoscale, we hypothesize that these modifications will be reflected in the disorder strength. We demonstrate this by imaging the tissue microarray using a technique called Spatial Light Interference Microscopy (SLIM), which is a high-sensitivity QPI method, able to detect sub-nanometer optical pathlength fluctuations [5].

**Methods**

A schematic of the SLIM setup is shown in Fig 1A. The SLIM module is attached to a commercial phase contrast microscope (PCM). The lamp filament is imaged onto the condenser
annulus (Köhler illumination conditions) which is located at the front focal plane of the condenser lens. The specimen is located at the back focal plane of the condenser lens, and front focal plane of the objective. The scattered and unscattered lights are relayed by the objective and tube lenses. As a result, the expanded phase contrast image which has the intensity distribution in accordance with the phase contrast caused by the specimen is observed at the image plane. However, because the output of PCM is the qualitative phase image, the quantitative phase map caused by the specimen cannot be directly retrieved from this image. The function of SLIM module is to convert this qualitative phase image into a quantitative one by properly phase modulating the incident light with respect to the scattered light. The field at the image plane is Fourier transformed by the lens L1, such that the unscattered light can be spatially isolated from the scattered light. Since the unscattered light has the ring form, by displaying the corresponding ring pattern on the reflective liquid crystal phase modulator (LCPM), we insure that the scattered light remains unaffected. Four phase shifts are applied to the unscattered light at increments of $\pi/2$ rad. as shown in Fig 1B. The corresponding four images captured by the charge coupled device (CCD) are obtained as shown Fig 1C. Consequently, the quantitative phase image is retrieved as described in Ref. [5] and Fig 1D.

Fig 2A and 2B show the quantitative phase image and its expanded view of benign and malignant breast tissue samples, respectively. The samples comprised a tissue microarray (TMA) of cores constructed from breast tissue biopsies of 400 different patients. Each biopsy was formalin fixed and paraffin embedded before sectioning it into slices of 4 μm thickness.
each using a microtome. Two parallel, adjacent sections were selected from each biopsy and one of these sections was stained using H&E, leaving the other one unstained. Cores were then constructed for both the stained and unstained tissue, and these were mounted on separate slides after de-paraffinization, using xylene as the mounting medium. The stained samples were imaged using a bright-field microscope, and their images served as a reference for evaluating diagnosis on the unstained samples using SLIM. The slides were obtained from our collaborating pathologist, Dr. Andre Kajdacsy-Balla, at the University of Illinois at Chicago. Each patient consented to their tissue samples being used as a part of the study and the process of obtaining consent was approved by the Institute Review Board (IRB Protocol Number 2010–0519) at University of Illinois at Chicago (UIC). The data analysis was conducted on the samples at the University of Illinois at Urbana-Champaign (UIUC) after all patient identifiers had been removed. The procedures used in this study for conducting experiments using human subjects were also approved by the institute review board at UIUC (IRB Protocol Number 13900).
By definition, the disorder strength map, \( L_d(x, y) \), is expressed as:

\[
L_d(x, y) = \langle \Delta n(x, y)^2 \rangle_w L,
\]

(2)

Here, \( \langle \ldots \rangle_w \) denotes the average within the window of interest, \( \Delta \) means the difference from its average, i.e., \( \Delta n(x, y) = n(x, y) - \langle n(x, y) \rangle_w \), and \( L \) is the spatial autocorrelation length. Fig 3A shows the quantitative phase image \( \phi(x, y) \), which contains information about the spatial variation of the refractive index change of tissues as expressed by Eq 1. The local variance and average of the phase have the form, respectively,

\[
\langle (\Delta \phi(x, y))^2 \rangle_w = \left( \frac{2\pi}{\lambda} \right)^2 \langle (\Delta n(x, y))^2 \rangle_w
\]

(3a)

and

\[
\langle \phi(x, y) \rangle_w^2 = \left( \frac{2\pi}{\lambda} L \right)^2 n_{\text{mean}}^2
\]

(3b)

Here, \( n_{\text{mean}} \) is the average of the refractive index in the tissue. Thus, the local refractive index fluctuation map, which is independent of the thickness, can be computed as [32]

\[
\langle \Delta n(x, y)^2 \rangle_w = \frac{\langle (\Delta \phi(x, y))^2 \rangle_w}{\langle \phi(x, y) \rangle_w^2} n_{\text{mean}}^2.
\]

(4)

Therefore, we can rewrite Eq 2 and obtain the final form to calculate the disorder strength map from the quantitative phase image as [32]

\[
L_d(x, y) = \langle (\Delta \phi(x, y))^2 \rangle_w n_{\text{mean}} L,
\]

(5)

In our calculation, we used a window of 5×5 pixels (0.125 \( \mu \)m/pixel). Fig 3B and 3C show the example of the calculation result of \( \langle \phi(x, y) \rangle_w^2 \) and \( \langle (\Delta \phi(x, y))^2 \rangle_w \), respectively. Also, from these two images, we can obtain \( \langle (\Delta \phi(x, y))^2 \rangle_w / \langle \phi(x, y) \rangle_w^2 \) as shown in Fig 3D. Since our interest is the fluctuation only in the tissue region, the background pixels were excluded. In our calculation, the pixels which satisfy \( \langle \phi(x, y) \rangle_w \) < 0.075 rad. are treated as background pixels. Here, we note that the selected threshold value of 0.075 rad. is about 3 times larger than the standard deviation of \( \phi(x, y) \) in an arbitrary selected background region. Fig 3E shows \( \langle (\Delta \phi(x, y))^2 \rangle_w / \langle \phi(x, y) \rangle_w^2 \) after applying this mask. Furthermore, because the very large value of \( \langle (\Delta \phi(x, y))^2 \rangle_w / \langle \phi(x, y) \rangle_w^2 \) are observed in the small area including the edge of the tissue where the thickness in the area might not be constant, the pixels having the value larger than 0.21 are filtered out as shown in Fig 3E. Consequently, the disorder strength can be calculated using the resulting phase image. Fig 3G shows the normalized 2D spatial autocorrelation function of \( \phi(x, y) \), \( \Gamma(x, y) \). From this, we re-plot the normalized spatial autocorrelation function in terms of \( r = (x^2 + y^2)^{1/2} \) as shown in Fig 3H. Then, the spatial autocorrelation length, \( L_s \), is defined as the half width at 1/e of the maximum, i.e., \( \Gamma(r = L_s) = 1/e \).

**Results**

Fig 4A and 4B shows the disorder strength maps of benign and malignant samples, respectively. It can be seen that the disorder strength in the malignant sample is larger than that in the benign sample. Also, we can find that the disorder strength obtained in our calculation is
Fig 3. Procedures. (A) Original phase image. (B) Local phase average map. (C) Local phase variance map. (D) Local phase fluctuation map. (E) Local phase fluctuation map with background reduction mask. (F) Local phase fluctuation map with edge reduction filter. (G) 2D spatial autocorrelation. (H) 1D spatial autocorrelation.

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of the order of 1 μm which is higher than that obtained in previous studies [21, 32]. This is likely caused by the difference in contrast between different techniques and different nature of the samples. Laser QPI methods are known to produce lower contrast phase images, ϕ(x, y). As a result, Δϕ(x, y) has much smaller values in this case. Furthermore, using smaller windows for averaging also results in lower Δϕ(x, y) values. Images obtained by SLIM has higher contrast than those obtained by other imaging systems, which result in higher phase variance. In addition, tissue biopsy cores generally have a complex structures compared with single cells which were used in the previous works [32, 33]. Fig 5 shows the averaged disorder strength across the tissue area. The error bar in the figure denotes the standard error in 20 samples.
each. The p-value between the benign and malignant samples using two-sided Wilcoxon rank-sum test was 0.0066. The results indicate that there are statistically significant differences between these two groups, therefore, the disorder strength can be utilized as a marker for tissue screening. As demonstrated in [32, 33], measurement of disorder strength can inform on the mechanical properties of a biological specimen and our results motivate further studies investigating how tissue mechanics vary with disease progression, with disorder strength used as a convenient metric.

Summary

In summary, we showed that the disorder strength measured from QPI is a quantitative marker of malignancy that can be used to classify benign and malignant breast cores. This marker, based on refractive index fluctuations that are indicative of the disorder strength, is obtained here from unlabeled tissue samples, meaning that it is not affected by stain variation across different samples.

Finally, we note that previous publications have shown that, from quantitative phase images of tissue slices, one can extract the scattering mean free path and anisotropy factor of the bulk [34, 35]. This result, known as the scattering phase theorem, has led to multiple SLIM studies of using scattering parameters for diagnosis and prognosis [10, 12–15, 36]. Specifically, the scattering mean free path, \( l_s \), relates to the phase variance as \( l_s = L / \langle \Delta \phi(x, y)^2 \rangle_w \) [35]. Therefore, from Eq 5, we see that, averaging over the same spatial scale, the disorder strength and scattering mean free path are simply inversely proportional, \( L_d \propto 1 / l_s \). The physical significance of this result is straightforward: higher tissue disorder generates stronger scattering, which implies shorter \( l_s \). It is, thus, not surprising that both parameters have been used successfully in cancer pathology, as they both report on tissue inhomogeneity. SLIM provides a robust, high-throughput approach to imaging histology slides. Recent advances in SLIM data acquisition allowed us to image an entire microscope slide, containing hundreds of tissue cores, at 0.5 \( \mu \)m transverse resolution in 45 min, while maintaining the sub-nanometer path-length sensitivity [16]. Because SLIM can be implemented as an upgrade of the existing microscopes, we anticipate that it can be plugged into the existing pathology workflow and help solve many problems of clinical importance.

Supporting information

S1 Fig. Quantitative phase images of cores used in this study.
(TIF)

S2 Fig. Disorder strength maps of cores used in this study.
(TIF)

S1 Table. Disorder strength of each core.
(XLSX)

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