Water transport in protoplanetary disks and the hydrogen isotopic composition of chondrites

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Abstract

The D/H ratios of carbonaceous chondrites, believed to reflect the hydrogen isotopic composition of water in the inner early solar system, are intermediate between the protosolar value and that of most comets. The isotopic composition of cometary water has been accounted for by several models where the isotopic composition of water vapor evolved by isotopic exchange with hydrogen gas in the protoplanetary disk. However, the position and the large range of variation of the distribution of D/H ratios in carbonaceous chondrites have yet to be explained. In this paper, we assume that the D/H composition of cometary ice was achieved in the disk building phase and model the further isotopic evolution of water in the inner disk in the classical T Tauri stage. Reaction kinetics compel isotopic exchange between water and hydrogen gas to stop at ~500 K, well inside the snow line. However, the equilibrated water can be transported to the snow line (and beyond) via turbulent diffusion and consequently mix with isotopically comet-like water. Thus the competition between outward diffusion and net inward advection established an isotopic gradient, which is at the origin of the large isotopic variations in the carbonaceous chondrites and other water-bearing objects accreted in the protoplanetary disk.

Under certain simplifying assumptions, we calculate analytically the probability distribution function of the D/H ratio of ice accreted in planetesimals and compare it with observational data. The distribution is found to essentially depend on two parameters: the radial Schmidt number $S_{Cr}$, which ratios the efficiencies of angular momentum transport and turbulent diffusion, and the range of heliocentric distances over which currently sampled chondrite parent bodies were accreted. The minimum D/H ratio of the distribution corresponds to the composition of water condensed at the snow line, which is a function of both the composition of equilibrated water having diffused through alteration of originally anhydrous silicates by water presumably incorporated as ice along with rock during accretion (Brearley 2003; Ghosh et al. 2006).

The measured D/H ratios of bulk carbonaceous chondrites (see Fig. 5), generally thought to reflect that of accreted water (but see Alexander et al. 2012b), span a range of $120 \times 10^{-6}$ to $230 \times 10^{-6}$ (excluding CR chondrites). The distribution, which is skewed to heavy isotopic compositions, has a mean $(156 \pm 3) \times 10^{-6}$ close to the $(149 \pm 3) \times 10^{-6}$ estimated for the bulk Earth (Lecuyer et al. 1998) — consistent with a chondritic source for terrestrial water. The D/H ratios of carbonaceous chondrites is systematically lower than that exhibited by many Oort-cloud comets ($296 \pm 25 \times 10^{-6}$, Hartogh et al. 2011), although D/H ratios of $(161 \pm 24) \times 10^{-6}$ and $(206 \pm 22) \times 10^{-6}$ have been determined for Jupiter-family comet Hartley 2 and Oort-cloud comet Garradd, respectively (Hartogh et al. 2011; Bockelée-Morvan et al. 2012). The composition of interplanetary dust particles, though broadly similar to that of carbonaceous chondrites (e.g. Engrand and Maurette 1998; Bradley 2005), has a significant tail extending to cometary values and beyond. Both chondritic and cometary domains of variation are markedly distinct from both the estimated protosolar value $(20 \pm 3.5) \times 10^{-6}$, (Geiss and Gloeckler 2003), dominated by the isotopic composition of hydrogen gas, and the high values (D/H $\gtrsim 10^{-3}$) determined in molecular clouds for molecules other than H$_2$, consistent with predictions from ion-molecule

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\textsuperscript{1}And carbonaceous chondrite-like microclasts in howardites (Gounelle et al. 2005).
reactions (see e.g. Robert 2006). However, high D/H values \(\gtrsim 2 \times 10^{-5}\) have been reported at the micrometer scale in clays of the Semarkona chondrite (Piani et al. 2012; Piani 2012) and may reflect the composition of pristine interstellar ice grains.

In the protoplanetary disk, the D/H ratio of water evolves mainly through isotopic exchange with the hydrogen gas (whose composition remains essentially fixed at the protosolar value because it contains the bulk of the H of the system), that is, via the reaction:

\[
\text{HDO} + \text{H}_2 \rightleftharpoons \text{H}_2\text{O} + \text{HD}
\]

The goal of this paper is to calculate analytically the distribution of D/H ratios of chondritic water that results from this picture and compare it to the observational data, in order to constrain the model parameters. In particular, the calculation will be constrained by the asymmetrical shape of the distribution and its position relative to cometary values. We stress that here the cometary value is a starting, observationally given parameter of the model. Our model does not aim at reproducing the composition of comets in contrast to the studies of Drouart et al. (1999); Mousis et al. (2000); Hersant et al. (2001); Yang et al. 2012: rather, in complementarity to those, it focuses on chondrite parent bodies, that is, the inner regions of the solar system. Also in complementarity to these numerical studies, our work, in being analytic in nature, allows us to nail down, under certain simplifying assumptions, the relevant parameters (essentially two) that govern the distribution of chondritic D/H ratios, namely: the range of heliocentric distances sampled by chondrites and the radial Schmidt number—which essentially ratios

\[
\text{HDO} + \text{H}_2 \rightleftharpoons \text{H}_2\text{O} + \text{HD}
\]
the efficiencies of angular momentum transport and turbulent diffusion. We will find that low values of the radial Schmidt number yield D/H variations consistent with observations. The paper is organized as follows: We describe the model assumptions in Section 2, present and discuss the results in Sections 3 and 4, respectively. In Section 5, we conclude. For the sake of clarity, specific derivations are deferred to appendices.

2. Modeling

In this section, we introduce our notations and modeling principles. We successively consider the disk model (Section 2.1), the transport of water (Section 2.2), its D/H ratio (Section 2.3) and our prescription for accretion and delivery to Earth (Section 2.4).

2.1. The disk

We consider an axisymmetric, vertically isothermal turbulent disk. The disk is assumed to have a stationary surface density profile in its inner regions such that its (radially constant) mass accretion rate \( \dot{M} \) is given by:

\[
\dot{M} = -2\pi R \Sigma \alpha_k \equiv 3\pi \Sigma \alpha_k \frac{c_s^2}{\Omega} \tag{2}
\]

with \( R \) the heliocentric distance, \( \Sigma \) the surface density, \( \alpha_k \) the vertically averaged radial velocity of the gas, \( \alpha \) the vertically averaged turbulence parameter, \( \Omega \) the Keplerian angular velocity and \( c_s = \sqrt{k_B T/m} \) the isothermal sound speed—where \( k_B \) and \( m \) are the Boltzmann constant and the mean molecular mass, respectively, and \( T \) the temperature. The steady-state approximation is expected to hold so long the viscous evolution timescale,

\[
t_{\text{vis}}(R) \equiv \frac{R^2}{3 \alpha c_s^2 \Omega} = 0.05 \text{ Ma} R_{\text{AU}}^{-1/2} \left( \frac{300 \text{ K}}{T} \right) \left( \frac{10^{-3}}{\alpha} \right), \tag{3}
\]

is shorter than the disk’s age in the regions of interest. Similarly to Drouart et al. (1999) and Hersant et al. (2001)—see also Hartmann et al. (1998) and Chambers (2009)—we take the mass accretion rate to evolve in time at2

\[
\dot{M} = \frac{\dot{M}_0}{(1 + t_{\text{vis}})^{3/2}} \tag{4}
\]

where \( \dot{M}_0 \) is the mass accretion rate at some initial time \( t = 0 \) and \( t_{\text{vis}} \) an evolution timescale (\( t_0 > t_{\text{vis}}(R) \)).

We adopt the same temperature prescription as in Jacquet et al. (2012):

\[
T = \max \left( \frac{3}{128 \pi^2} \frac{k m}{\sigma_{\text{SB}} k_B \alpha} M^2 \Omega^3 \right)^{1/5} \frac{1}{f_T R_{\text{AU}}^{-1/2}}, \tag{5}
\]

with \( k \) the specific opacity, \( \sigma_{\text{SB}} \) the Stefan-Boltzmann constant, \( T_0 = 280 \text{ K}, f_T \) a dimensionless constant parameter (for which we will adopt a fiducial value of 0.5) and \( R_{\text{AU}} \equiv R/(1 \text{ AU}) \). This prescription essentially states that inner disk regions are dominated by the dissipation of turbulence (“viscous heating”), which decreases with decreasing accretion rate, whereas the outer disk regions are dominated by reprocessing of solar radiation. Hence, the snow line (at heliocentric distance \( R_{\text{cond}} \)), which corresponds to a fixed temperature of \( T_{\text{cond}} = 170 \text{ K} \), recedes toward the Sun with the passage of time.

For simplicity, we will assume that \( \alpha \) and \( \kappa \) are constant throughout the disk’s extent and evolution.

2.2. Water transport

We now turn to the transport of water. We distinguish between nebular and accreted water. Nebular water is water dynamically coupled to the gas, whether as water vapor or ice-bearing grains, and behaves as part of the disk. It is predominantly gaseous inside the snow line and solid outside it. Accreted water refers to water retrieved from the gas by incorporation in planetesimals or comets.

We first focus on the dynamics of nebular water. Since it behaves as a passive contaminant in the gas, the evolution equation of its surface density \( \Sigma_{\text{H}_2\text{O}} \) reads (e.g. Ciesla and Cuzzi 2006):

\[
\frac{\partial \Sigma_{\text{H}_2\text{O}}}{\partial t} + \frac{1}{R} \frac{\partial}{\partial R} \left( R \left( \Sigma_{\text{H}_2\text{O}} + \frac{1}{2} \frac{\partial}{\partial R} \left( \frac{\Sigma_{\text{H}_2\text{O}}}{2} \right) \right) \right) = -S_{\text{coll}} \tag{6}
\]

with \( S_{\text{coll}} \) the sink term resulting from collisions — both coagulation and shattering processes (contributing positively and negatively to it, respectively) —, and \( \delta g \) a dimensionless number (of order \( \alpha \)) parameterizing turbulent diffusion. We neglect any gas-solid drift induced by gas drag (we shall return to this assumption in Section 2.2).

If coagulation and shattering can be ignored, it is straightforward to see that \( \Sigma_{\text{H}_2\text{O}} \propto \Sigma \) is a solution of the equation. This should remain a reasonable approximation for coagulation timescales longer than \( t_{\text{vis}} \). There is evidence suggesting that accretion was indeed quite inefficient/slow in the early solar system: age dating of chondrite components and studies of the thermal evolution of their parent bodies are consistent with accretion being a protracted process on a few-Ma timescale (e.g. Villeneuve et al. 2009; Grimm and McSween 1989; Kleine et al. 2008; Connelly et al. 2012) and the total mass of the current planetary system (see e.g. Hayashi 1981) is one order of magnitude lower than the nonvolatile content of disks at the end of the infall phase (e.g. Yang and Ciesla 2012) assuming a solar metallicity. We shall thus assume that accretion was inefficient and ignores its feedback on the dynamics of nebular water so that \( \epsilon_{\text{H}_2\text{O}} \equiv \Sigma_{\text{H}_2\text{O}}/\Sigma \) can be considered constant (we shall return to this issue in Section 4).

2.3. Hydrogen isotopic composition of water

In this paper, we assume that the D/H ratio of water is dictated by isotopic exchange between originally isotopically heavy (comet-like) water and isotopically light hydrogen gas (e.g. Drouart et al. 1999; Mousis et al. 2008; Hersant et al.
To make the problem analytically tractable, we circumvent an accurate treatment of reaction kinetics by schematically distinguishing between two types of water: cometary water is water that has never experienced temperatures in excess of a “reaction temperature” $T_{\text{reac}}$ during the classical T Tauri stage of the disk, and is assumed to retain a relatively heavy D/H ratio denoted $(D/H)_h$; equilibrated water, on the other hand, is water that did experience temperatures above $T_{\text{reac}}$ and therefore has a D/H ratio set to a fixed value $(D/H)_i$ through isotopic exchange with hydrogen gas (a justification for this treatment based on reaction kinetics is provided in Appendix A). $T_{\text{reac}}$, $(D/H)_i$ and $(D/H)_h$ are fixed parameters of the model and are assigned values of $500 \text{ K}$, $4 \times 10^{-6}$ and $300 \times 10^{-6}$ for them, respectively (see Appendix B). The value of $200 \times 10^{-6}$ corresponds to the maximum D/H ratio that can be reached by water in equilibrium with molecular hydrogen. Indeed, although enrichment in D could be in principle higher at lower equilibration temperature, slow kinetics of the isotopic exchange reaction prevent this equilibrium from being actually attained below $T_{\text{reac}}$.

We denote by $R_{\text{reac}}$ the heliocentric distance where $T = T_{\text{reac}}$, which is given by:

$$R_{\text{reac}} = \left( \frac{3 k \rho T_{\text{reac}}}{G M_\odot} \right)^{3/2} \frac{2}{3} \left( \frac{3 k \rho T_{\text{reac}}}{G M_\odot} \right)^{3/2}$$

$$= 1 \cdot \frac{M_\odot(T_{\text{reac}})}{\alpha} \frac{10^{-3}}{\alpha} \left( \frac{500 \text{ K}}{T_{\text{reac}}} \right)^{10/9}$$

with $M_\odot \equiv M/(10^{-8} \text{ M}_\odot \cdot \text{a}^{-1})$, in the viscous-dominated regime. The mass accretion rate where $R_{\text{reac}}$ enters the irradiation-dominated regime (see equation (C.4)) is in our model:

$$M_{\text{reac}} = \left( \frac{3 \pi \rho_0 T_{\text{reac}}^{3} \sigma_{SB} k \rho_0 f_J T_0 \alpha}{2 \pi} \right)^{1/2}$$

$$= \frac{4 \times 10^{-11} \text{ M}_\odot \cdot \text{a}^{-1}}{\alpha} \left( \frac{0.5 \text{ m}^2/\text{kg}}{\alpha} \right)^{1/2} \left( \frac{f_J}{0.5} \right)^{9/2}$$

$$\left( \frac{500 \text{ K}}{T_{\text{reac}}} \right)^{1/2}$$

where we have introduced the radial Schmidt number

$$S_{CR} = \frac{\alpha}{\sigma_R}$$

We will henceforth adopt this solution. In other words, we assume that the radial distribution of equilibrated water undergoes a quasi-static evolution as the mass accretion rate (and thus $R_{\text{reac}}$) decreases.

In this case, the D/H ratio of the total nebular water is given by

$$\left( \frac{D}{H} \right)_{\text{H}}(R, t) = \left( \frac{D}{H} \right)_{\text{H}} - \left( \frac{D}{H} \right)_{\text{H}} \left( \frac{R_{\text{reac}}(t)}{R} \right)^{3 S_{CR}/2}.$$ (11)

Thus, D/H is a monotonically increasing function both of heliocentric distance and time (as over time M and hence $R_{\text{reac}}$ decrease). This is plotted in Fig. 2 and 3.

2.4. Accretion and delivery to Earth of water-bearing chondrites

At this point, we have wholly prescribed the isotopic and transport properties of nebular water in our model. We have yet to relate this nebular water to the D/H distribution of chondrites.

We first need to make a prescription for coagulation/shattering, which determines the rate at which water is incorporated in chondritic bodies. Similarly to Cassen (1996) (see also Ciesla and Cuzzi 2006, Weidenschilling 2004), we posit a collision term of the form

$$S_{\text{coll}}(R, t) = \frac{\Sigma_{\text{H}_2}\Omega_{\text{coll}}(R)}{\Sigma_{\text{H}_2}} \theta(R - R_{\text{cond}}(t)),$$ (12)

where we use the fact that D/H $\ll 1$. 

[Figure 2: D/H ratio (expressed in parts per million (ppm)) of water as a function of heliocentric distance in a steady disk, for three values of the radial Schmidt number $S_{CR}$. In the “reaction zone”, delimited by a vertical dashed line (“equilibration line”), equilibrium isotopic fractionation with hydrogen gas is assumed; beyond, mixing with cometary water controls the D/H ratio (equation (11)). We have taken $M = 10^{-8} \text{ M}_\odot / \text{a}$, $\alpha = 10^{-10}$, $\kappa = 0.5 \text{ m}^2/\text{kg}$, $f_J = 0.5$. The smaller the $S_{CR}$, the more efficient radial mixing is. The position of the snow line (where water condenses) is indicated by a vertical dotted line: water is gaseous inside the snow line and solid outside.]

[Diagram showing D/H ratio as a function of heliocentric distance in AU, with three curves corresponding to different values of $S_{CR}$. The snow line is indicated by a vertical dotted line.]

[Equation (9) is shown: $\Sigma_{\text{H}_2}$ is the surface density of equilibrated water, $\Sigma_{\text{H}_2}$ is governed by the same equation as total water, i.e. equation (6) with $\Sigma_{\text{H}_2}$ replaced by $\Sigma_{\text{H}_2}$. A stationary solution to this equation, expected to be attained by $R_{\text{reac}}$, is given by Clarke and Pringle 1981, Stevenson 1990, see also Appendix A.]
with the coagulation timescale $t_{\text{coag}}(R)$ taken to scale like the local orbital timescale $(\Omega^{-1})$, $\theta$ the Heaviside function defined by

$$\theta(z) = \begin{cases} 
0 & \text{if } z < 0 \\
1 & \text{if } z \geq 0 
\end{cases}$$

We thus consider that water is accreted solely as ice.

We finally need to prescribe the delivery of accreted material to the Earth as a function of the heliocentric distance of initial agglomeration. While this step encompasses a variety of processes such as drift of meter-sized boulders, orbital evolution of parent bodies and eventually ejected meteoroids, we will be content in assuming a uniform probability of delivery of material to Earth up to a maximum initial heliocentric distance $R_{\text{max}}$. In other words, the distribution we are calculating will be representative of water ice accreted inside $R_{\text{max}}$. If the asteroid main belt accreted in situ, $R_{\text{max}}$ could be taken to correspond to its outer edge, near 3 AU. If, on the other hand, significant redistribution of planetesimals occurred, e.g. during the “Grand Tack” studied by Walsh et al. (2011), $R_{\text{max}}$ could be considerably larger.

3. Results

Under the above hypotheses, meteoritic water, having been accreted from a range of heliocentric distances (between the snow line and $R_{\text{max}}$) and at various times, will necessarily exhibit a range of D/H ratios and one can define a probability distribution function (PDF) for that quantity. The derivation and the expression of the PDF are presented in Appendix C and plots of it are shown in Fig. 4. It is notable that they are independent of $\alpha$, $t_0$, $t_{\text{coag}}(1 \text{ AU})$ $\mathcal{E}_{\text{H,O}}$ and $\kappa$ and depend on $f_r$, $T_{\text{cond}}$, $T_{\text{reac}}$, $(\text{D/H})_{\text{h}}$, $(\text{D/H})_{\text{l}}$, $R_{\text{max}}$ and $\text{Sc}_R$, of which only the latter two are considered free parameters.

Distributions exhibit a minimum cutoff value $(\text{D/H})_{\text{min},0}$ (see equation (C.8)). This minimum value of the distribution stems from the constraint that the accreted water be condensed, and...
corresponds to the hydrogen isotopic composition of water at the snow line. It is thus governed by isotope exchange kinetics (which determines the composition and origin of equilibrated water) and radial transport to the snow line (which determines the proportion of equilibrated water there) alike. It is noteworthy that the D/H ratio at the snow line does not evolve with time (so long it is in the viscous-heating dominated temperature region), as it only depends on the ratio \( T_{\text{cond}} / T_{\text{reac}} \) (see equation (C.5)).

As is apparent on each panel of Fig. 4, low values of \((D/H)_{\text{min,0}}\) are associated with efficient radial mixing (enabling a high proportion of equilibrated water at the snow line), that is, a small radial Schmidt number, through the relationship (using equation (C.8)):

\[
Sc_R = \frac{3}{5} \ln \left( \frac{(D/H)_{\text{H}_2O} - (D/H)_{\text{max}}}{(D/H)_{\text{H}_2O} - (D/H)_{\text{f}}} \right) \ln \left( \frac{T_{\text{cond}}}{T_{\text{reac}}} \right) \quad (14)
\]

For our fiducial parameters, if we adopt \((D/H)_{\text{min,0}} = 120 \times 10^{-6}\) from the observed PDF of D/H in carbonaceous chondrites, we obtain \(Sc_R = 0.2\).

A low value of \(Sc_R\) is also needed if one is to recover the positive skewness of the observed PDF (with a negative slope over most of the range of D/H values). Indeed, equation (C.3) indicates that the PDF has an overall dependence in \((D/H)_{\text{H}_2O} - (D/H)_{\text{max}})^{1/(\alpha Sc_R)}\), notwithstanding “second-order” modifications imposed by the constraint \(R_{\text{cond}} < R < R_{\text{max}}\) and the changes in the temperature regime. This imposes an overall decreasing trend if \(Sc_R \lesssim 1/3\). Efficient transport indeed means that the D/H ratio will be close to that at the snow line for a significant fraction of the outer disk, hence the dominance of this value in the PDF.

By comparing the two panels of Fig. 4, it is also apparent that the PDF is also more skewed toward higher D/H ratio if \(R_{\text{max}}\) increases, as is expected from the monotonic increase of D/H with increasing heliocentric distance in our model. The maximum value \((D/H)_{\text{max, f}}\) (see equation (C.11)) is related to \(R_{\text{max}}\) through the relationship (injecting equation (14) into equation (C.11)):

\[
R_{\text{max, f}} = \left( \frac{f_T \tau_0}{T_{\text{reac}}} \right)^2 \exp \left( \frac{10 \ln \left( \frac{T_{\text{max}}}{T_{\text{cond}}} \right)}{9} \ln \left( \frac{(D/H)_{\text{H}_2O} - (D/H)_{\text{min, f}}}{(D/H)_{\text{H}_2O} - (D/H)_{\text{max, f}}} \right) \right) \quad (15)
\]

If we adopt \((D/H)_{\text{max, f}} = 230 \times 10^{-6}\), one obtains \(R_{\text{max}} = 6\) AU. \(R_{\text{max}}\) as expressed above is however quite sensitive to the assumed parameters, and as such our calculation would not conclusively discriminate between \textit{in situ} formation of the asteroid main belt and widespread redistribution [Walsh et al. 2011]. Note that the evaluations of both \(Sc_R\) and \(R_{\text{max}}\) in equations (14) and (15) are independent of our prescriptions of accretion of solids or the functional form of \(Mt(t)\).

In Fig. 5, we have plotted the theoretical PDF with the \(Sc_R\) and \(R_{\text{max}}\) evaluated above (which by construction adjust the PDF to the minimum and maximum observed values and the histogram of the latter (observed) data). The shape of the observed PDF is reproduced qualitatively (though not quantitatively), with (i) a peak near the lower end of the distribution and (ii) a tail toward high D/H ratios. The peak corresponds to D/H ratios near the snow line, which dominate the distribution because accretion is most efficient there (because of shorter dynamical timescales and higher surface densities) than further from the Sun and also because efficient outward transport has almost homogenized the D/H ratios to the snow line value over an extensive region beyond it. The tail corresponds to water ice accreted some distance beyond the snow line, until the maximum heliocentric radius sampled.

However, the match is not quantitative, as the observed PDF is more peaked (around D/H = 150 \times 10^{-6}) than the theoretical prediction. Certainly, the simplifications used in the model (e.g. constant \(\alpha\), prescription of delivery to Earth etc.) prevent it from yielding realistic PDFs and only allow a proof-of-concept use. We shall now discuss implications of these results as well as assess the limitations of our treatment.

4. Discussion

4.1. Implications

From the above results, it appears that the distribution of D/H ratios of carbonaceous chondrites can be accounted for in a scenario of isotopic exchange with hydrogen gas, with cometary D/H values prevailing at large heliocentric distances, under the condition that the radial Schmidt number \(Sc_R\) be small (\(\lesssim 0.3\)).

\[\text{Note that this inequality does not depend on the prescription we have adopted for } Mt(t) \text{ but does depend on the power law for the irradiation-}
\]

\[\text{dominated temperature regime and that of the coagulation timescale: for } T = R^{-4} \text{ and }\tau_{\text{coag}} = R^{4}, \text{ the inequality becomes } Sc_R \lesssim (2(\alpha - q) - 1)/3 \text{ (going back to equation} (C.1)\]

\[\text{\textit{Figure 5: Probability distribution function of D/H values in bulk carbonaceous chondrites (CI, CO, CV, CM) compared to the theoretical PDF adjusted to fit the minimum and maximum of the distribution. The comparison is warranted only if isotopic exchange with organic matter on the parent body is negligible. Data from Kerber} (1985), Kolodny et al. (1980), Boato (1954), Robert and Epstein (1982), McNaughton et al. (1982), Yang and Epstein (1983), Pearson et al. (2001), Alexander et al. (2012).}\]
The peak value of the carbonaceous chondrite population would be essentially dictated by the isotopic composition of water near the snow line, where accretion of condensed water would be most efficient.

The low values inferred for ScR would not only have enhanced outward transport of equilibrated water, but also that of higher-temperature components as well (e.g. Bockelée-Morvan et al. 2002). This could account for the high-temperature minerals, including calcium-aluminum-rich inclusions (CAIs) and chondrule fragments identified in comet Wild 2 samples (Zolensky et al. 2006; Bridges et al. 2012) and also the relatively high abundances of CAIs in carbonaceous chondrites (see Jacquet et al. 2012).

If mixing was as efficient as inferred above, the D/H ratio could have been significantly lower than (D/H)H even at a few tens of AU, depending on time (see Fig. 2). Thus, comets may have formed with D/H ratios lower than (D/H)H (the limit at large heliocentric distances), which would account for the emerging range in measured D/H ratios of cometary water (Hartogh et al. 2011; Bockelée-Morvan et al. 2012), consistent with the idea of an asteroid-comet continuum (Gounelle et al. 2008; Briani et al. 2011). Even the $300 \times 10^{-4}$ value adopted for (D/H)H on the basis of measurements of known comets could then actually be a lower bound of its real value.

4.2. Modeling caveats

Of course the validity of the conclusions of this study can only be as good as that of its underlying assumptions.

First, the quasi-static approximation we have used requires, as we recall from Section 2.2, that the viscous timescale $t_{vis}(R)$ be short relative to the time of chondrite accretion and that of evolution of the mass accretion rate. In a dead zone, whose existence we have inferred above, $\alpha$ would likely be small, around $10^{-4}$ (e.g. Fleming and Stone 2003; Iignar and Nelson 2008; Oishi and Mac Low 2009; Turner et al. 2010), so that $t_{vis}$ would be longer than our nominal evaluation in equation (3), but at $R = 3$ AU, it would be ~1 Ma, still shorter than the accretion time of chondrites after the start of the solar system (~1-5 Ma, see e.g. Villeneuve et al. 2009; Connelly et al. 2012). Admittedly, the timescale constraint would be quite marginally satisfied, so that, conceivably, future re-examination of this problem in time-dependent simulations of disks with dead zones, with self-consistently evaluated $\alpha$ (see e.g. Zhu et al. 2010), could unveil new interesting effects. Nonetheless, this would not affect our conclusion that MRI-turbulent disk models, with higher $\alpha$—hence largely satisfying the timescale constraint—and ScR, cannot reproduce the D/H ratio of chondrites and our inference of the presence of dead zone thus appears robust in this respect.

Our steady-state disk model neglects photoevaporation during the bulk of the disk’s lifetime. However, if, as argued by Desch (2007), the disk was subject to intense photoevaporation from the outset, the net gas flow could have been outward, and equilibrated water would have reached the snow line almost undiluted; i.e. water at the snow line would have a D/H ratio close to (D/H)$_H$ ~ $40 \times 10^{-6}$. If such isotopically light preaccretionary water compositions were to be found in the future, this would be a possibility worth investigating; however, to date, such isotopic compositions have not been measured.

In this work, nebular water has been assumed to be dynamically coupled to the gas. Depending on the fragmentation and the bouncing barriers (e.g. Zsom et al. 2010; Birnstiel et al. 2012), it is however conceivable that ice-bearing particles grow to millimeter-size and beyond so that drift due to gas drag would be significant (see equation (A.5)) before they are incorporated in planetesimals. This would likely lead to significant enhancements of water abundance inside and at the snow line, and depletions further outwards (e.g. Cuzzi and Zahnle 2004).
From equation (A.8) derived in Appendix A, it can be seen that the fraction of equilibrated water would be lower, and thus D/H higher, than under our tight coupling calculation, because of increased import of “cometary water”. One example of this effect is shown in Fig. 6 using the parameters inferred from this study. While the effect might be limited for the carbonaceous chondrites which we have focused on—for which Jacquet et al. (2012) inferred that millimeter-sized components were not significantly drifting—, it would certainly accelerate the convergence of the D/H ratio toward its asymptotic value in the comet-forming region (for $S_R > 1$, see Appendix A). This could account for the apparent carbonaceous chondrite/comet hydrogen isotopic dichotomy, in the sense that relatively little material with intermediate composition would then exist (but does exist, as emphasized at the end of Section 4.1). However, regardless of the actual quantitative importance of radial drift, it must be noted that inasmuch as nebular water inside the snow line would be in vapor state—even meter-sized solids would lose their water by vaporization before they can travel much inward of it (Cuzzi and Zahnle 2004) — and thus continue to be tightly coupled to the gas, the transport of equilibrated water until the snow line would be unchanged (see equation A.8) — save for some transition period preceding establishment of the quasi-steady regime. Therefore, our estimate of $S_R$ from the minimum D/H of the distribution (established at the snow line) would be unaffected and is thus robust in this regard too.

We have also argued that accretion was inefficient, allowing us to ignore feedback on the transport of nebular water. If this approximation were not to hold, rapid accretion of planetesimals at the snow line could progressively deplete the inner solar system in water (e.g. Ciesla and Cuzzi 2006). Although, again, this would likely not affect the D/H ratio at the snow line, the effects on the shape of the PDF have yet to be determined by dedicated numerical simulations including both coagulation and shattering (see Yang et al. 2012).

### 4.3. On the interpretation of D/H chondrite data

In this work, we have compared our PDF of the isotopic composition of water to bulk chondrite compositions (see Fig. 5), and, in doing so, implicitly assumed that the latter reflected the composition of pre-accretionary water now locked in hydrated silicates. However, hydrated silicates are not the only contributors to the hydrogen budget of carbonaceous chondrites, as the latter also contain organic matter. The rationale for making this identification nonetheless is that inasmuch organic matter does not account for more than 10% of the hydrogen, at their presently measured D/H ratios (mostly $\leq 400 \times 10^{-6}$—still excluding CR chondrites—; Alexander et al. (2010)), the incurred shifts to the isotopic composition would be small ($\lesssim 20 \times 10^{-6}$; Robert 2006) compared to the observed range of D/H ratios. However, this ignores the possibility of isotopic exchange between organic matter and water on the parent body, in which case the observed composition might have been much more D-rich initially than presently measured. In fact, Alexander et al. (2012b) showed that the D/H ratio of bulk carbonaceous chondrites correlated positively with the C/H ratio, and interpreting this as a mixing trend, extrapolated an initial D/H ratio for organic matter comparable to that of CR chondrites ($\approx 700 \times 10^{-6}$), and consequently, a lighter isotopic composition for pre-accretionary water, e.g. $(86.5 \pm 3.5) \times 10^{-6}$ for CM chondrite. In that case, while (direct) comparison of the theoretical PDF with the histogram plotted in Fig. 5 would no longer make sense, $(D/H)_{min,0}$ would be constrained to be lower than this latter value, and our formalism would thus constrain $S_R$ to be $\lesssim 0.1$ (see equation (14)), that is, a yet more efficient radial diffusion would be indicated.

It must be cautioned, though, that in situ observations of CI, CM and CR chondrite matrices have revealed little evidence of isotopic exchange between the isotopically heterogeneous organic matter and the intermixed hydrous minerals (Remusat et al. 2010) and organic matter in the least aqueously altered CM chondrite Paris has an hydrogen isotopic signature indistinguishable of that of the other CM (Remusat et al. 2011). One possible explanation for the D/H - C/H correlation of Alexander et al. (2012b) could be that the cometary water endmember was somehow coupled to D-rich organic matter in the disk, consistent with the high carbon contents of cometary grains (e.g. Wozniakiewicz et al. 2012). In that case, the mixing trend would not actually extrapolate to the composition of the organic matter but to that of the resulting composite (water + organics) C- and D-rich endmember. In this picture, the hydrogen isotopic signatures of organic matter and hydrated silicates could be actually largely pristine, as inferred by Remusat et al. (2010). Whatever that may be, and whether D/H ratios of bulk carbonaceous chondrites truly reflect the D/H ratios of preaccretionary water or only provide upper limits, we stress that low Schmidt numbers are robustly required in the framework of our formalism.

While the present work has mainly focused on carbonaceous chondrites, it is noteworthy that non-carbonaceous chondrites are generally richer in deuterium than the former (e.g. Robert 2006; Alexander et al. 2012b). As the D/H ratio of nebular water increases with time in our scenario, this could imply that they accreted later than the former, as suggested by Jacquet et al. (2012) based on the modeled redistribution of chondrite components in the disk. Conceivably, radial drift, as alluded to in the preceding subsection, which would be most pronounced as the coupling of the grains with the less dense gas would be looser then, might have contributed to significant enhancements of the D/H ratios for them. In fact, Jacquet et al. (2012) specifically inferred that millimeter-size components were significantly drifting for these chondrites, and from equation (A.8), the nebular water should be isotopically close to cometary values, which appears to be the case for clays from unequilibrated ordinary chondrites (e.g. Robert 2006; Alexander et al. 2012b).

---

5 This would incidentally explain some low-D/H point measurements in L3 chondrites (Deolake et al. 1998).

6 Alexander et al. (2012b) suggest that the high D/H ratios of these meteorites could be due to oxidation of metallic iron by water producing isotopically light hydrogen gas escaping from the system. However, while this may have affected metamorphosed chondrites (Alexander et al. 2010; McCauley et al. 2008), the most unequilibrated ordinary chondrites also show these high values, with considerable heterogeneity consistent with the pristinity of this signature (Piani 2012).
A later formation of the non-carbonaceous chondrites would avoid the alternative possibility of an accretion further from the Sun than carbonaceous chondrites, which would run counter to the observed distribution of asteroid classes (e.g. Burbine et al. 2008). A later formation time could also account for the high D/H values of CR chondrites too—consistent with their young chondrule Al-Mg ages (Kita and Ushikubo 2012) —which could mark an intermediate status between the other carbonaceous and the non-carbonaceous chondrites—along with their rather low refractory inclusions abundance, their limited refractory element enrichment relative to Mg, and their relatively heavy oxygen isotopic composition (Scott and Krot 2003).

5. Summary

We have considered a simplified analytic model for water transport and isotopic evolution in an evolving disk based on the following main assumptions:

(i) The regions of interest of the disk are approximated by a stationary model, with a constant turbulence parameter $\alpha$.

(ii) Accretion is inefficient and does not significantly affect the transport of nebular water.

(iii) Water far from the Sun is assumed to have the same D/H ratio as cometary water, and any batch of water having experienced temperatures above a “reaction temperature” $T_{\text{react}}$ has had its D/H reset to a fixed value (D/H).

(iv) Accretion is modeled by a coagulation timescale scaling with the orbital period and water is incorporated as ice only. A uniform probability of delivery to Earth is applied to agglomeration locations up to a maximum heliocentric distance $R_{\text{max}}$.

In this model, the D/H ratio of water is an increasing function of time and heliocentric distance. After integration over time, the probability distribution function (PDF) of the D/H ratio in accreted water is found to depend essentially on $R_{\text{max}}$ and (most sensitively) on the radial Schmidt number $Sc_R \equiv a/\delta R$ with $\delta R$ parameterizing the diffusivity. The minimum cutoff of the PDF is determined by isotopic composition of water at the snow line, while the isotopically heavy tail is dictated by $R_{\text{max}}$.

It appears that the model is able to broadly account for the observed PDF in carbonaceous chondrites if low values of $Sc_R$ (around 0.1-0.3)—i.e. efficient outward diffusion—are assumed in order to reproduce the low D/H values of most chondrites and the positive skewness of the observed distribution. This would be most consistent with hydrodynamical turbulence as expected to prevail in the dead zone of the protoplanetary disk. Efficient outward diffusion would also have enabled the transport of high-temperature minerals to comets. The high D/H ratios in CR chondrites and non-carbonaceous chondrites could indicate an accretion later than most carbonaceous chondrites.

The effects of radial drift and higher accretion efficiencies on the transport of water and its hydrogen isotopic composition have yet to be investigated.

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Appendix A. Diffusion of equilibrated water in disks

In this appendix, we calculate the steady-state profile of nebular water concentration and its equilibrated fraction. To allow discussion of the tight coupling assumption in Section 4 we take into account the finite size of ice-bearing particles beyond the snow line, and thence the effects of gas drag, so that their velocity becomes, ignoring any feedback of the solids on the gas (e.g. Birnstiel et al. 2010):

$$v_R = \frac{1}{1 + St} \left( - \frac{3}{\Sigma R^{1/2}} \frac{\partial}{\partial R} \left( R^{1/2} \Sigma v \right) + \frac{\tau}{P \rho} \frac{\partial P}{\partial R} \right), \quad (A.1)$$

with $\nu = \alpha c_s^2/\Omega$ the turbulent viscosity, $\tau$ the gas drag stopping time, $St \equiv \Omega \tau$ the Stokes number, and $P$ and $\rho$ the gas pressure and density, respectively.

In steady state, the mass accretion rate of nebular water

$$M_{H_2O} = 2\pi R \left( -\Sigma H_2O v_R + D_R \Sigma \frac{\partial}{\partial R} \left( \Sigma H_2O \right) \right), \quad (A.2)$$

is constant. We have introduced the diffusion coefficient modified by finite particle size as $D_R \equiv \frac{\delta R c_s^2}{\Omega}$. (A.3)

Equation (A.2) may be viewed as a first-order ordinary differential equation in $\Sigma H_2O/\Sigma$. It is noteworthy that the corresponding homogeneous equation is the equation governing the transport of equilibrated water, since its concentration vanishes at infinity, so that:

$$\frac{\Sigma H_2O_{\text{eq}}}{\Sigma} \propto \exp \left( \int \frac{v_R}{D_R} dR \right) \propto \exp \left( \int \frac{S_R d\rho}{\rho} dR \right) \propto \left( \Sigma \nu R^{1/2} \right)^{\delta R/\delta \Sigma} \quad (A.4)$$

where the second proportionality relationship assumes that $Sc_R$ is radially constant and we have coined $S_R = St/\delta R$ which is a measure of gas-grain decoupling (Jacquet et al. 2012). In the Epstein drag regime, for spherical grains of density $\rho_s$ and radius $a$ (averaged over the size distribution), we have:

$$S_R \equiv \frac{\pi}{2} \frac{\rho_s a^2}{\Sigma \delta R} = \frac{3\pi^2 Sc_R \rho_s a^2}{4 \rho M \Omega} = 0.1 \frac{Sc_R^{1/2}}{M_{\text{Sun}}} \left( \frac{\rho_s a}{1 \text{ kg/m}^2} \right) \left( \frac{T}{300 \text{ K}} \right), \quad (A.5)$$

where the last two equations pertain to a steady disk as assumed in the main text. Note that the normalizing value $\rho_s a = 1 \text{ kg/m}^2$ corresponds to millimeter-sized grains (the typical size of non-matrix chondrite components).
By requiring that \( \Sigma_{\text{H}_2\text{O}}/\Sigma \) does not diverge at the disk’s inner edge (whose heliocentric distance we denote by \( R_{\text{eq}} \), taken to be zero in the main text), equation (A.2) may be then integrated as:

\[
\frac{\Sigma_{\text{H}_2\text{O}}}{\Sigma} = \exp \left( \int_{R_{\text{in}}}^{R} \frac{\nu_g R}{D} dR \right) \int_{R_{\text{in}}}^{R} \exp \left( - \frac{\int_{R_{\text{in}}}^{R} \nu_g R dR'}{2\pi R' \Sigma D_R} \right) \frac{M_{\text{H}_2\text{O}} dR'}{2\pi R'^2 \Sigma D_R} \]  
(A.6)

For \( S_R \ll 1 \) (in particular inside the snow line where \( S_R = 0 \)), this is a constant, and for \( S_R \gg 1 \approx \epsilon \), it falls off as \( 1/S_R \). Then, the fraction of equilibrated water is:

\[
\frac{\Sigma_{\text{H}_2\text{Oeq}}}{\Sigma_{\text{H}_2\text{O}}} = \left[ \int_{R_{\text{in}}}^{R} \exp \left( - \frac{\int_{R_{\text{in}}}^{R} \nu_g R dR'}{2\pi R' \Sigma D_R} \right) \frac{dR'}{R' \Sigma D_R} \right]^{-1} \]  
(A.7)

Enforcing that the left-hand-side be unity at \( R = R_{\text{reac}} \), this becomes:

\[
\frac{\Sigma_{\text{H}_2\text{Oeq}}}{\Sigma_{\text{H}_2\text{O}}} = \frac{2}{3 \Sigma c_R} \left( \sqrt{R_{\text{reac}}^2 - \sqrt{R_{\text{in}}^2}} \right)^{3 \Sigma c} \exp \left( - \int_{R_{\text{reac}}}^{R} S_R \frac{\partial P}{\partial R} dR' \left( 1 + \frac{\sigma_T}{T} \right) \frac{dR'}{\sqrt{R'}} \right) \]  

For \( S_R \ll 1 \), this amounts to equation (2) for \( R_{\text{in}} \ll R_{\text{reac}} < R \).

### Appendix B. Kinetics of water-hydrogen isotopic exchange

Ignoring transport, and given that \( \text{D/H} \ll 1 \) and \( \text{H}_2\text{O}/\text{H}_2 \ll 1 \), the equation governing the evolution of D/H of water may be written as [Leculuse and Robertson (1994)]:

\[
\frac{d}{dt} \left( \frac{D}{H} \right) = k^-(T) n_H \left[ \left( \frac{D}{H} \right)_{\text{eq}} (T) - \left( \frac{D}{H} \right) \right] \]  
(B.1)

with \( n_H \), the number density of hydrogen molecules, \( (\text{D}/\text{H})_{\text{eq}} \) the equilibrium values (see e.g. [Richet et al. 1977]) and the rate constant

\[
k^-(T) = 2 \times 10^{-28} \exp \left( \frac{-5170}{T} \right) \text{m}^3/\text{s}. \]  
(B.2)

Given that, in our steady-state model, the midplane number density can be expressed as a function of temperature (assumed to be vertically constant) as

\[ n_H = \frac{\Sigma \Omega}{\sqrt{2\pi m c_s}} = \frac{16}{9} \frac{3}{M \alpha} \left( \frac{2T^{11/2}}{\pi k_B^2 m} \right)^{1/6} \left( \frac{\sigma_{SB}}{k} \right)^{2/3} \]  
(B.3)

the characteristic equilibration timescale resulting from equation (B.1) is:

\[
t_{\text{eq}} = \frac{1}{k^-(T)n_H} = 0.1 M \alpha \exp \left( \frac{-5170}{T} \right)^{1/3} \left( \frac{\alpha M_{\text{reac}, \text{K}}}{10^{-3}} \right)^{1/3} \left( \frac{\kappa}{0.5 \text{ m}^2/\text{kg}} \right)^{2/3} \]  
(B.4)

This is a sharply decreasing function of temperature. While, at high temperature, \( t_{\text{eq}} \) is short compared to the transport timescale \( t_{\text{vis}} \) so that water vapor and hydrogen gas can be considered in equilibrium, at lower temperature (at larger heliocentric distances), \( t_{\text{eq}} \) becomes long compared to \( t_{\text{vis}} \) and isotopic exchange is essentially quenched. The temperature \( T_{\text{reac}} \) marking the transition between the two regimes can be determined by setting:

\[
t_{\text{eq}}(T_{\text{reac}}) \equiv t_{\text{vis}}(T_{\text{reac}}). \]  
(B.5)

Water originating from inside \( \text{H}_2\text{O} \) (“equilibrated water”) will then essentially have the isotopic composition it had when it last equilibrated with hydrogen gas, i.e. at \( T = T_{\text{reac}} \), that is, its D/H ratio will be \( (\text{D}/\text{H})_{\text{eq}}(T_{\text{reac}}) \).

Numerically, equation (B.5) can be expressed as:

\[
\frac{\exp \left( \frac{-5170}{T_{\text{reac,K}}} \right)}{T_{5/18}^{1/9}} = 5 \times 10^3 \frac{10^{-3}}{M_{1/9}^{1/9}} \frac{0.5}{\alpha \text{ m}^2/\text{kg}} \]  
(B.6)

The left-hand-side being a sharply decreasing function of \( T_{\text{reac}} \), the sensitivity on \( M \) is completely negligible and that on \( \alpha \) is also fairly weak. We shall thus adopt the solution of this equation for \( \alpha = 10^{-3} \), \( M = 10^{-8} \text{ M}_{\odot}/\text{a} \), \( \kappa = 0.5 \text{ m}^2/\text{kg} \), which is \( T_{\text{reac}} = 500 \text{ K} \). Adopting a protosolar D/H ratio (for the \( \text{H}_2\text{O} \) gas) of \( 20 \pm 3.5 \times 10^{-6} \) [Geiss and Gloeckler 2003], the fractionation factor given by [Richet et al. 1977] yields \( (\text{D}/\text{H})_l \approx 40 \times 10^{-6} \).

### Appendix C. Calculation of the PDF of D/H

In this appendix, we detail the calculation of the PDF of the D/H ratio of meteoritic water. We will here denote D/H by \( x \) for the sake of legibility of the equations.
With the model set up in Section 2, the mass of meteoritic water with D/H ratio between $x$ and $x + dx$ is

$$\int_0^{x_{\text{max}}} S_{\text{cell}}(R(x, t), t)2\pi R(x, t) \frac{\partial R}{\partial x} dx \theta(R_{\text{max}} - R(x, t)) dt \propto f(x) dx \quad (C.1)$$

where $f(x)$ is the normalized probability density function of bulk chondrites in terms of D/H ratio, $t = 0$ is taken to correspond to the time where $R_{\text{cond}} = R_{\text{max}}$, i.e. the earliest possible time where water can condense and be accreted inside $R_{\text{max}}$, corresponding to the mass accretion rate

$$M_0 = \left( \frac{128\pi^2 \sigma_{SB} k_B T_\text{cond}^5}{3 km\Omega(T_{\text{cond}}/10 \text{AU})^3} \right)^{1/2} \approx 1.5 \times 10^{-7} M_0, \alpha^{-1} \left( \frac{0.5 \text{ m}^2/\text{kg}}{10^{-3} \kappa} \right)^{1/2} \left( \frac{T_{\text{cond}}}{170 \text{ K}} \right)^{5/2} \left( \frac{R_{\text{max}}}{10 \text{ AU}} \right)^{9/4} \quad (C.2)$$

Using the assumed constancies of $\epsilon_{H_2O}$, $\Omega_{\text{cond}}(R)$, $\alpha$, $Sc_R$ and using equation (2), we have:

$$f(x) \propto \int_0^{x_{\text{max}}} \frac{\dot{M}(t)}{R_{\text{rec}}(t)} R(t, x, t) \theta(R_{\text{max}} - R(t, x, t)) \theta(R(t, x, t) - R_{\text{cond}}(t)) dt \propto (x_h - x)^{1/9} \left[ \frac{\dot{M}(t)}{\dot{M}_0} \right]^{1/2} \min \left( \frac{M_h(x)}{M(t)} , 1 \right) \quad (C.3)$$

with $t_{\text{min}}(x)$ and $t_{\text{max}}(x)$ determined by the conditions $R < R_{\text{max}}$ and $R > R_{\text{cond}}$, respectively, $M_0(t)$ the mass accretion rate for which $x(R_0) = x$, where $R_0$ is defined as the heliocentric distance of the transition between the viscous-heating- and the irradiation-dominated regimes and is given by (see equation (5)):

$$R_{\text{br, AU}} = \left( \frac{3}{128\pi^2 \sigma_{SB} k_B T_\text{cond}^5} \left( \frac{f_T T_0^5}{f_T} \right) \right)^{1/2} \approx 3 M_{\text{g}} \frac{128\pi^2 \sigma_{SB} k_B T_\text{cond}^5}{f_T T_0^5} \left( \frac{\epsilon}{10^{-3} \kappa} \right)^{1/2} \left( \frac{\Omega}{1 \text{AU}} \right)^{1/2} \left( \frac{M_0}{M_0} \right)^{1/2} \quad (C.4)$$

with $\Omega_0 \equiv \Omega(1 \text{AU})$. The “min(...)” factor in equation (C.3) is unity when $R(t, x, t)$ is in the irradiation-dominated regime.

Before proceeding to the result, we coin a few additional notations and then proceed to the integration. Fig. C.7 may help the reader to visualize the situation in the D/H - time space.

For a given mass accretion rate, the minimum and maximum value of D/H dictated by the conditions $R_{\text{cond}} \leq R \leq R_{\text{max}}$ are:

$$x_{\text{min}}(M) = \begin{cases} x_h - (x_h - x_l) \left( \frac{T_{\text{cond}}}{T_{\text{cond}}} \right)^{3Sc_a/2} & \text{if } T_{\text{br}} \leq T_{\text{cond}} \\ x_h - (x_h - x_l) \left( \frac{T_{\text{cond}}}{T_{\text{cond}}} \right)^{3Sc_a/2} & \text{if } T_{\text{cond}} < T_{\text{br}} < T_{\text{rec}} \\ x_h - (x_h - x_l) \left( \frac{T_{\text{cond}}}{T_{\text{cond}}} \right)^{3Sc_a/2} & \text{if } T_{\text{br}} \geq T_{\text{rec}} \end{cases} \quad (C.5)$$

and

$$x_{\text{max}}(M) = x_h - (x_h - x_l) \left( \frac{R_{\text{rec}}(M)}{R_{\text{max}}} \right)^{3Sc_a/2} \quad (C.6)$$

The D/H ratio at $R = R_0$ (for $M \geq M_{\text{rec}}$) is:

$$x_{\text{br}}(M) = x_h - (x_h - x_l) \left( \frac{128\pi^2 \sigma_{SB} k_B \alpha (f_T T_0)^9}{3 km M^2 \Omega(T_{\text{cond}}/10 \text{AU})^3} \right)^{5Sc_a/12} \quad (C.7)$$

To all these, a “br” subscript will be added if evaluated for $M = M_0$ and “f” for $M = M_{\text{frec}}$. Hence,

$$x_{\text{min},0} = x_{\text{max},0} = x_h - (x_h - x_l) \left( \frac{T_{\text{cond}}}{T_{\text{rec}}} \right)^{5Sc_a/2} \quad (C.8)$$

$$x_{\text{br},0} = x_h - (x_h - x_l) \left( \frac{128\pi^2 \sigma_{SB} k_B \alpha (f_T T_0)^9}{3 km M^2 \Omega(T_{\text{cond}}/10 \text{AU})^3} \right)^{5Sc_a/2} \quad (C.9)$$

$$x_{\text{min},f} = x_h - (x_h - x_l) \left( \frac{T_{\text{cond}}}{T_{\text{rec}}} \right)^{3Sc_a} \quad (C.10)$$

$$x_{\text{max},f} = x_h - (x_h - x_l) \left( \frac{T_{\text{cond}}}{T_{\text{rec}}} \right)^{3Sc_a} \quad (C.11)$$

where $T_{\text{rec}}(M_{\text{rec}}) \equiv f_T T_0 R_{\text{max, AU}}$ is the irradiation temperature at heliocentric distance $R_{\text{max}}$.

We will also need the D/H ratio when $R = R_{\text{max}}$, which is given by:

$$x_{\text{max},f} = x_h - (x_h - x_l) \left( \frac{T_{\text{cond}}(R_{\text{max}})}{T_{\text{rec}}} \right)^{5Sc_a} \quad (C.12)$$

and the ratio $M_{\text{frec}}/M_0$ between the final and the starting mass accretion rate:

$$\frac{M_{\text{frec}}}{M_0} = \left( \frac{T_{\text{rec}}(R_{\text{max}})}{T_{\text{cond}}(R_{\text{max}})} \right)^{1/2} \quad (C.13)$$

With all these notations, we can express the result of the integration in equation (C.3) as:

$$f(x) = C(x_h - x)^{1/9} \left( \frac{x_h - x_{\text{br},0}}{x_h - x} \right)^{1/15Sc_a} \left( 1 - \frac{M_{\text{rec}}}{M_0} \right)^{1/9} \frac{1}{S(x)} \quad (C.14)$$

for $x_{\text{min},0} \leq x \leq x_{\text{max},f}$, and

$$f(x) = C(x_h - x)^{1/9} \left( \frac{x_h - x_{\text{br},0}}{x_h - x} \right)^{1/15Sc_a} \left( \frac{x_h - x_{\text{min},0}}{x_h - x} \right)^{1/9} \frac{1}{S(x)} \quad (C.15)$$

for $x_{\text{max},f} \leq x \leq x_{\text{max},f}$. 

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Here, $C$ is a normalization factor given by
\[
C = \left[ \frac{S_c(x_0 - x)^{1/3}}{3S_c} \left( \frac{12}{\tau_{\text{cond}}^{0.5T_{1/18}}} - 18 \frac{\tau_{\text{cond}}^{0.5T_{1/18}}}{\tau_{\text{cond}}^{0.5T_{1/18}}} + 10 \frac{\tau_{\text{cond}}^{0.5T_{1/18}}}{\tau_{\text{cond}}^{0.5T_{1/18}}} - \frac{\tau_{\text{cond}}^{0.5T_{1/18}}}{\tau_{\text{cond}}^{0.5T_{1/18}}} \right) \right]^{-1} \tag{C.16}
\]
and $S(x)$ is defined as
\[
S(x) = \begin{cases} 
\frac{x - x}{x - x_{\text{min}}} & \text{if } x < x_{\text{min}}, \\
1 & \text{if } x \geq x_{\text{min}}.
\end{cases} \tag{C.17}
\]

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