Comparison Method of PI, PID and Fuzzy Logic Controller to Maintain Speed Stability in Single Phase Induction Motors

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Abstract—Induction motor speed control is one of the operating conditions that are often used so that feedback with a low error rate is required. To achieve this control aim, PI and PID controls have been widely implemented for single phase induction motors. This control is commonly dictated by parameters of Kp, Ki and Kd. PI and PID controls can cover a variety of desired response conditions, but these controls still have weaknesses in the tuning process. The tuning process used still has a fairly large error value. So in this case it is required an intelligent controls to meet the desired motor speed response specifications. The performance of motor speed regulation was evaluated using a comparison between PI and PID control with Fuzzy in a closed loop. With a setting point of 1500 rpm, for PI control, with Kp = 7.32 and Ki = 0.005 can obtain motor speeds up to 1499 rpm. While PID control with Kp = 0.95, Ki = 0.005 and Kd = 0.04 can obtain similar speeds of 1492 rpm. Fuzzy control can obtain an output of 1490 rpm. Fuzzy control is able to produce a settling time of 0.25 seconds and a steady error of 0.67%.

Keywords—Fuzzy Logic Controller, PI Controller, PID Controller, Single Phase Induction Motor

1. Introduction

Single phase induction motors are the most common motors used in home appliances [1]. Of course, the speed level of the motor will have an effect on supporting the common jobs of household activities itself. However, the speed setting on the induction motor is still a problem. The objective of controlling induction motor speed is to achieve the maximum torque and efficiency [2]. However, speed control gives the opposite side to the properties of the induction motor. Normally, an induction motor has a difficulty maintaining their speed. It delivers a quite high error rate when the induction motor speed setting is operated with an open system. Error (e(t)) is the difference between the reference value and the measurable corresponding value [3]. One way to overcome this error is by providing a control/technique control as feedback [4]. From several applied applications, PI and PID controller are two controllers that are often employ due to the simple controller structure and practical. PI and PID controller has three parameters used, the variable parameters namely proportional, integral and derivative (Kp, Ki, Kd) [5]. PI parameters can be determined via parameter tuning. Common method used as a tuning is analytics method. In general, it is often difficult to determine the optimal PI and PID parameters with analytics method, therefore the output response is resulting in a closed system will be inappropriate (causing a large enough oscillation), even though PI and PID controller are expected to obtain a stable output response [6].

Currently, there has been several developments of smart controller, for example a fuzzy logic controller [7]. Fuzzy logic controller is a controller that utilizes the system decision-making [8]. Several references show the output of Fuzzy controller provides low rise time with no overshoot excess and low steady state error allows rare oscillations. It allows to control a single phase induction motor to be able operate optimally in every condition.

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II. Research Methodology

A. Motor Speed Control Method

A voltage source with a sinusoidal wave as the reference signal is applied, this voltage source uses a triangular wave as a carrier signal [9]. This carrier signal frequency is called switching frequency. The switching frequency can determine the length of time on the pulse when open the foot gate on the switching component besides that it also affects the output voltage drop of the inverter [10].

![Figure 1. Scheme of SPWM in the MATLAB Simulation](image)

In Figure 2, it can be seen that there are two fcn inputs, the fcn is used to form a reference signal (sine signal). The reference signal can be formed through the equation (1) and (2).

\[
\begin{align*}
\text{Fcn1} &= u[1]*\sin(u[2]*2\pi*u[3]) \\
\text{Fcn2} &= u[1]*\sin(u[2]*2\pi*u[3]+\pi)
\end{align*}
\]

Where:
- \(U[1]\) = MA (modulation index of the SPWM signal)
- \(U[2]\) = frequency
- \(U[3]\) = clock

To be able to run the v/f method, the first thing to do is determine the setting point of the plant.

\[
\begin{align*}
\text{NS} &= \frac{120 \text{ Fc}}{P} \\
1500 &= \frac{120 \text{ Fc}}{2} \\
\text{Fc} &= 25 \text{ Hz}
\end{align*}
\]

Where:
- \(\text{NS}\) = the expected setting point
- \(\text{Fc}\) = frequency control
- \(P\) = the number of motor poles

After getting the \(\text{Fc}\) value, it will be compared with the frequency. Therefore, it could obtain the MA value.

\[
\begin{align*}
\text{MA} &= \frac{\text{Fc}}{\text{Ff}}
\end{align*}
\]

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This MA will be the basis for the formation of the pulse signal which will form the duty cycle. (When MA = 1, duty cycle = 100%) \[11\]. The formation of duty cycle will be affecting the output voltage of the inverter. Which is the input for the motor.

\[
\begin{align*}
Vo &= MA \times Vs \\
Vo &= 0.5 \times 220 \\
Vo &= 110 \text{ V}
\end{align*}
\]

From equation (5) and (3) it can be seen that the input voltage of motor is 110 V, and the frequency is 25 Hz. This can be proven by the V/f method, which has a ratio equal to 4.4. This ratio is a fixed ratio, regardless of the value of the voltage and frequency.

**B. Power Converter**

Single phase inverter is used to convert DC voltage into AC voltage \[12\]. Single phase inverter consists of 4 switching components, either IGBT or Mosfet \[13\]. The output voltage of inverter is in the form of an AC voltage, but this wave still has a sufficiently large THD of current and voltage, so that it is not a pure sinusoidal wave \[14\].

Figure 2 is shown a single phase full bridge inverter, which consists of 4 switch devices. It can be seen in the single phase inverter schematic circuit, that there is a freewheeling diode which is installed in parallel to each of the inverter electronic switch devices. This diode serves to prevent the emergence of reverse current from inductive loads to the inverter voltage source which can damage electronic switch devices used in single phase inverters.

The inverter design functions to produce voltage 220 Volt AC with a frequency 50 Hz \[15\]. The switching method generated by the driver on the ignition signal of single phase inverter using IC IR 2111 is the unipolar method (PWM). In the driver single phase inverter circuit, before the signal enters IC IR 2111 there is an optocoupler, namely IC FOD 3182 which functions as a safety between the driver circuit and the microcontroller as well as signal conditioning to produce a pulse voltage 12 Volts as an ignition signal on the electronic switch contained in the single phase inverter.

**C. Control Feedback**

This part discusses the design of 3 controllers; PI, PID and Fuzzy Logic Controller.

1. **Design of PI Controller**

Calculating PI controller will use an analytic method. The main purpose is to determine the parameters of Kp and Ki of the plant \[16\]. Figure 3 is a response curve for design PI controller using the analytic method.

\[
\text{Figure 2. Single phase inverter circuit}
\]

\[
\text{Figure 3. Response curve PI controller with Analytic method}
\]
From the curve, it can be known that the single phase induction motor has nominal speed of 3000 rpm.

Steady State (Yss)

\[ Y_{ss} = 2999 \text{ rpm} \]

Time Settling (ts)

\[ t_s = 0.78 \text{ s} \]

Setting point (Xss)

\[ X_{ss} = 1500 \text{ rpm} \]

\[ K = \frac{Y_{ss}}{X_{ss}} \]  
\[ K = \frac{2999}{1500} \]
\[ K = 1.99 \]

\[ T = t_s \]
\[ T = \frac{0.78}{5} \]
\[ T = 0.156 \text{ s} \]

\( \tau = \tau_i = 0.156 \text{ s} \)

Open Loop Transfer Function PI:

\[ C(s) \frac{U(s)}{U(s)} = \frac{K}{T s + 1} \]
\[ C(s) \frac{U(s)}{U(s)} = \frac{1.99}{0.156 s + 1} \]

If it aims to serve this plant in a double faster, it needs new value of T.

\[ T' = \frac{0.78}{10} \]
\[ T' = 0.078 \]
\[ \tau' = \frac{0.078}{5} \]
\[ \tau' = 0.0156 \text{ s} \]

\[ K_{p} = \frac{\tau}{\tau' \times K} \]
\[ K_{p} = \frac{0.156}{0.0156 \times 1.99} \]
\[ K_{p} = 5.032 \]

\[ K_{i} = \frac{K_{p}}{\tau} \]
\[ K_{i} = \frac{5.032}{0.156} \]
\[ K_{i} = 32.25 \]

2. Design of PID Controller

Calculating PID controller will use an analytic method. The main purpose is to determine the parameters of Kp, Ki and Kd of the plant [17]. Data Yss, Xss, ts, and T for PID controller are same with PI controller because it still uses the same plan.

\[ T = \frac{t_s}{3} \]  
\[ T = 0.26 \text{ s} \]

Find Value of \( \alpha \):

\[ \alpha = 3.84 \]

Find value of \( \omega_d \):

\[ \omega_d = 4.6 \]

From the graphic we know that time peak of the plant happen at 0.68s. It means, time peak occurs before settling time.

Find \( \zeta \) on and \( \xi \):

\[ \zeta_{on} = \alpha \]  
\[ \omega_d^2 = \omega_n^2 (1-\xi^2) \]
\[ 21.16 = \omega_n^2 - \omega_n^2 \xi^2 \]
\[ 21.16 = \omega_n^2 - 14.74 \]
\[ \omega_n^2 = 35.9 \]
\[ \omega_n = 5.99 \text{ rad/s} \]

\[ \xi_{on} = 3.84 \]

\[ \xi(5,99) = 3.84 \]

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\( \xi = 0.64 \)

Open Loop Transfer Function PID:

\[
\frac{C(s)}{U(s)} = \frac{K}{(\xi \omega_n s)^2 + (2 \xi \omega_n s) + 1}
\]

\[
\frac{C(s)}{U(s)} = \frac{1.99}{(0.0275s)^2 + (0.215s) + 1}
\]

Find value of \( \tau' \):

\[
\tau' = \frac{\xi \omega_n}{\tau_s}
\]

\[
\tau' = 0.78 \times \frac{2}{2} = 0.39
\]

Find value of \( \tau_i \):

\[
\tau_i = \frac{2 \times \xi}{\omega_n}
\]

\[
\tau_i = \frac{2 \times 0.64}{5.99} = 0.21
\]

Find value of \( \tau_d \):

\[
\tau_d = \frac{1}{\tau_i \times \omega_n^2}
\]

\[
\tau_d = \frac{1}{0.21 \times 5.99^2} = 0.13
\]

Find value of \( K_p \):

\[
K_p = \frac{1}{K} \times \frac{\tau}{\tau_i}
\]

\[
K_p = \frac{1}{1.99} \times \frac{0.26}{0.39} = 0.33
\]

Find value of \( K_i \):

\[
K_i = \frac{K_p}{\tau_i}
\]

\[
K_i = \frac{0.33}{0.21} = 1.57
\]

Find value of \( K_d \):

\[
K_d = K_p \times \tau_d
\]

3. Design of Fuzzy Logic Controller

Fuzzy logic controller uses Mamdani method with input variables FIS (Fuzzy Inference System) error and \( \Delta \) error [19]. Design Fuzzy logic controller describes the design of membership functions in input and output variables of the FIS and creates a basic rule [20]. Plot and parameter input variables FIS “error” are shown in Figure 4 and Table 1.

![Figure 4. Plot of the error membership function in the Mamdani method](image)

| Name            | Type    | Parameter          |
|-----------------|---------|--------------------|
| NB (Negative Big) | trapezoid | -2.2 -1 -0.7       |
| NM (Negative Medium) | triangle | -1 -0.65 -0.3     |
| NS (Negative Small) | triangle | -0.7 -0.35 0     |
| ZE (Zero)       | triangle | -0.2 0 0.2        |
| PS (Positive Small) | triangle | 0.035 0.7        |
| PM (Positive Medium) | triangle | 0.3 0.65 1      |
| PB (Positive Big) | trapezoid | 0.71 2.2        |

This value is obtained from the difference between setting point and speed read on the scope. Figure 5 shows the membership function “\( \Delta \) error” and Table 2 shows the parameter of the membership function “\( \Delta \) error”.

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This value is obtained from the difference between error and speed read. Furthermore, Figure 6 shows output fuzzy membership function and Table 3 shows output fuzzy membership function parameters.

This value is obtained from the difference between error and speed read. Furthermore, Figure 6 shows output fuzzy membership function and Table 3 shows output fuzzy membership function parameters.

Determining value of output fuzzy, it is adjusted to the expected setting point. For the rule base, the more rules that are applied, the higher the level of accuracy, so that many aspects are controlled [21].

### III. Results and Discussion

In this simulation, a feedback control is applied to adjust system response to suit the necessity of plant (motor). Table 5 shows the results of the test at close loop with PI controller.

In Table 5, it can be seen that the resulting error value is less than 1% and this number is considered successful for doing control.

Figure 7 shows a graph of the measured speed and reference speed in a close loop simulation test with PI controller. In the graph below, made a value 1500 rpm and the measured speed is 1502 rpm.
Figure 7. Graphic speed reference and measured speed with PI controller

Where:
Blue line : reference speed (setting point) 1500 rpm
Orange line: rated speed on the motor with a value 1502 rpm.

From the results with the PI controller, the system has a low error rate in speed regulation. Beside, with feedback control, speed response obtained has a lower oscillation rate than without giving control.

Next, a feedback control is employed to adjust system response to suit the necessity of plant (motor). Table 6 shows the results of the test at close loop with PID controller.

| Setting point (rpm) | Nm (rpm) | % Error |
|---------------------|----------|---------|
| 3000                | 2967     | 1.1%    |
| 2700                | 2671     | 1.0%    |
| 2400                | 2375     | 1.0%    |
| 2100                | 2043     | 2.7%    |
| 1700                | 1689     | 0.6%    |
| 1500                | 1498     | 0.1%    |

It can be seen in table 6 that the resulting steady error is greater than the PI controller, and the largest error reaches 2.7%. This number is quite large for a controller, because it is not close to the expected setting point.

Figure 8 shows a graph of the measured speed and reference speed in a close loop simulation test with PID controller. In the graph below, made a value 1500 rpm and the measured speed is 1498 rpm.

Figure 8. Graphic speed reference and measured speed with PID controller

Where:
Blue line : reference speed (setting point) 1500 rpm
Orange line: rated speed on the motor with a value 1502 rpm.

From the results of these data with the PID controller, the system has a higher error than PI controller in speed regulation. And based on Figure 8, the PID controller that used in this system has a larger settling time than the PI controller, but the system stability is better because the oscillations in some parts are lost.

On the PI and PID controllers some of the weaknesses can be seen, this can occur because of the improper tuning process carried out conventionally and in this system does not use variable come from calculations, these calculations are made as a benchmark for tuning new variable in order to produce better graphics.

To overcome these weaknesses, it will be juxtaposed with a fuzzy logic controller. This fuzzy does not use manual calculations. Table 7 shows the results of the test at close loop with fuzzy logic controller.

| Setting point (rpm) | Nm (rpm) | % Error |
|---------------------|----------|---------|

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In Table 7, it can be seen that the resulting error value is less than 1% and this number is considered successful for doing control.

Figure 9 shows a graph of the measured speed and reference speed in a close loop simulation test with Fuzzy logic controller. In the graph below, made a value 1500 rpm and the measured speed is 1493 rpm.

From the results of these data with the fuzzy logic controller, the system has a low error rate in speed regulation.

It can be seen in the Table 7 that there is an added setting point of 1200 rpm, it turns out that the fuzzy logic controller can still maintain the stability of the system. This can occur because the fuzzy logic controller has one pole so that it can freely control the system without depending on other poles. Difference with PI and PID, when they were given a setting point lower than the proper setting point (1500 rpm), they could not maintain their stability. This is because the control has more than one pole, so when from the beginning the setting point is designed, the controller will maintain the setting point only in that area. Figure 10 will show the comparison between the three controllers with variable speed.

| Set point (RPM) | PI  | PID  | Fuzzy |
|----------------|-----|------|-------|
| 1200           | 1798| 1794 | 1793  |
| 1500           | 1702| 1498 | 1493  |
| 1700           | 1656| 1689 | 1687  |
| 1800           | 1380| 1502 |       |

Figure 10. Comparison with variable speed

Where:
Blue line : Reference speed
Orange line: PI control
Green line : PID control
Pink line : Fuzzy control

Figure 10 is a comparison of variable speed. These variations are 1800 rpm, 1700 rpm and 1500 rpm. At 1500 rpm, the fuzzy control is the longest settling time control, however, these three controls can restore the speed to the expected setting point.

From Table 8 it can be seen that the data exhibit a setting point of control comparison varies over time. It also shows the time it takes for a control to re-adjust in the new setting point after it has been changed. It appears that the fuzzy control has a long time to return
after getting a disturbance. However, the three controls can still restore in steady state condition.

IV. Conclusion

From the results, it can be drawn several conclusions as follow:

1. For conventional controller, the tuning results are not the same as the calculation results (approaching).
2. Conventional controller (PI & PID), the setting point range is not as wide as fuzzy logic controller.
3. PI controller has number of KP = 7.32 and KI = 0.005. PI controller also has a result that carries a set point, the error is 0.1% and the settling time for this PI control is 0.20 seconds. However, the disadvantage of this control is that there is still some oscillation over time.
4. PID controller has number of KP = 0.95; KI = 0.005 and KD = 0.04. The control result of this PID is a single phase induction motor speed which has an error 0.1% against the setting point. The settling time of the PID controller is the longest of the other controllers, which is 0.51 seconds.
5. Fuzzy logic controller with 7 membership functions has the biggest error against the setting point, it is 0.4%. And the settling time after getting this fuzzy controller becomes 0.25 seconds. However, this fuzzy controller has the most stable speed among other controllers.

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