Pulsational instability of pre-main-sequence models from accreting protostars

I. Constraining the input physics for accretion with spectroscopic parameters and stellar pulsations

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ABSTRACT

Context. The picture of pre-main-sequence evolution is often simplified by the application of classical initial models. Such models have large initial radii and sufficient uniform contraction to make them fully convective, however, real stars are born as small protostellar seeds in collapsing molecular clouds and obtain their final mass by means of accretion.

Aims. We aim to constrain the input physics of accretion on protostellar seeds with the observed spectroscopic parameters and stellar pulsations of young stellar objects and pre-main-sequence stars.

Methods. We conducted a literature search for spectroscopic samples of young stellar objects and pre-main-sequence stars, including all previously known pulsators. The sample size of pulsating pre-main-sequence stars was increased by analysing TESS observations and presenting additional discoveries in the CoRoT data. We employed Modules for Experiments in Stellar Astrophysics and GYRE to calculate evolutionary tracks of accreting protostellar seeds in a constant accretion scenario, the subsequent pre-main-sequence evolution, and their pulsation properties. We then compared the results with the observations to constrain the input physics.

Results. We discuss 16 formerly unknown pulsating pre-main-sequence stars and candidates that are of any of the following type: slowly pulsating B-stars, δ Scuti, γ Doradus, or a δ Scuti - γ Doradus hybrid type. We find that evolutionary tracks with a mass accretion rate of $5 \times 10^{-6}$ $M_\odot$ yr$^{-1}$ and a fraction of injected accretion energy of $\beta = 0.1$ provide the best results for enveloping the spectroscopic parameters of pre-main-sequence stars in the constant accretion scenario. The calculated instability regions constrain the atmospheric boundary conditions to Eddington gray atmospheres. Here, we discuss the future potential for additional constraints by instability regions that are dependent on radial order. Finally, we present a possible candidate star for pulsations in M-type young stellar objects.

Conclusions. We show that evolutionary calculations of accreting protostellar seeds match the observed spectroscopic parameters of pre-main-sequence stars. Future observations that will allow for the identification of radial orders in particular will present opportunities for additional constraints.

Key words. asteroseismology – stars: oscillations – accretion, accretion disks – stars: formation – stars: pre-main sequence – stars: protostars

1. Introduction

Stellar structure and evolution is a colossally important topic, both observationally and theoretically. Owing to the vastly different evolutionary stages of stars, it is increasingly difficult to retain a unified picture of this phenomenon. Despite its role as a vital building block of stellar evolution, the pre-main-sequence evolution often falls victim to this circumstance. Stars do not merely pop up on the main sequence, but they are created as small stellar seeds (or second hydrostatic cores, see Larson 1969; Masunaga & Inutsuka 2000) from the collapse of molecular clouds, where the formation of stars is dependent on several parameters such as metallicity (Bate 2019). These seeds then continue to accrete material from their surroundings, most commonly from their embedded disks. Again, this process is dependent on the parameters of the surrounding material, leading to varying accretion rates for otherwise similar stellar seeds (Vorobyov & Basu 2010, 2015; Vorobyov et al. 2020).

Given that the physics governing early stellar evolution is very different, it is astonishing that the discussion of the pre-main sequence in the non-specialised community often has not substantially progressed since the pioneering works of Henyey et al. (1955), Hayashi (1961), and Iben (1965). While the formation of stars from accreting protostellar seeds in one dimensional (1D) stellar models has been an ongoing area of research for many years (Mercer-Smith et al. 1984; Palla & Stahler 1991; Hartmann & Kenyon 1996; Baraffe et al. 2009; Hosokawa et al. 2011; Vorobyov et al. 2017; Kunitsomo et al. 2017), it seems that this insight is still far from reaching the whole of the asteroseismic community. This series of papers aims to close the
gap between these two areas of research by combining state-of-the-art 1D pre-main-sequence models with asteroseismology.

Decades have passed since the first pre-main-sequence pulsators were discovered by Breger (1972). Today, it has become clear that slowly pulsating B-stars (SPBs), δ Scuti variables, and γ Doradus stars also exist in the pre-main-sequence phase of stellar evolution (see e.g., Ripepi et al. 2011; Gruber et al. 2012; Zwintz et al. 2013, 2014). As such, both gravity modes (g-modes) and pressure modes (p-modes) are common in stars even before the main sequence. The existence of solar-like oscillations in pre-main-sequence stars has been theoretically predicted (Samadi et al. 2005; Pinheiro 2008) and a first candidate was recently suggested by Mülher et al. (2021). In addition, bursts in accretion rate might lead to short-lived radial oscillations (Bastien et al. 2011).

The advent of space telescopes such as CoRoT (Avergne et al. 2009), Kepler (Borucki et al. 2010; Koch et al. 2010), and TESS (Ricker et al. 2015) and thanks to their stunning accuracies (Bastien et al. 2011) was recently suggested by Müllner et al. (2021). In addition, instabilities (Bastien et al. 2011) and gas (Alecian et al. 2013) and are often still in their pre-main-sequence phase of evolution. Hence, we added all stars, except the binaries, of this study to our sample. These are in total 65 stars.

Similarly, Fairlamb et al. (2015) conducted a spectroscopic study of Herbig AeBe stars. We excluded stars that the authors could not model successfully with magnetospheric accretion. Thus, we added 81 objects to our sample. The sample from Fairlamb et al. (2015) and Alecian et al. (2013) overlap, meaning that multiple stars are present in both surveys. In such a case, we use the stellar parameters provided in both studies as the measurements are obtained independently from each other.

Aidalman et al. (2018) obtained low resolution spectra of 68 B-type stars in the four open clusters: NGC 6087, NGC 6250, NGC 6383, and NGC 6530. The respective ages are ~55, ~6, ~3~10, and ~4~7 Myr (see Aidelman et al. 2018, for more detail and previous age estimates). Owing to the fast evolution toward the ZAMS of such intermediate mass stars, we omitted NGC 6087 because of its age (~55 Myr). The remaining 50 stars were then added to our sample of pre-main-sequence and early ZAMS stars.

Alecian et al. (2013) performed a high resolution spectropolarimetric survey of Herbig AeBe stars. The characteristics of Herbig AeBe stars suggests that they remain surrounded by dust and gas (Alecian et al. 2013) and are often still in their pre-main-sequence phase of evolution. Hence, we added all stars, except the binaries, of this study to our sample. These are in total 65 stars.

Frasca et al. (2017) obtained spectroscopy of young stellar objects in the ~2 Myr old Lupus star forming region. Their sample contains 104 young stellar objects, 89 of which are listed as members of Lupus. We therefore add these 89 stars to our sample of pre-main-sequence and early ZAMS stars.

Gutiérrez Albarrán et al. (2020) derived cluster ages and memberships of open clusters as part of the Gaia-ESO survey. Of the 20 clusters discussed in this work, three are young open clusters: ρ Oph, Cha I, and γ Vel with ages of 1~3, 2, and 10~20 Myr, respectively. A total of 45 stars are classified as members of one of these three young open clusters and thus we added them to our sample.

Da Rio et al. (2016) reported the results of infrared spectroscopy for pre-main-sequence stars in the Orion A molecular cloud. They obtained 2700 high resolution spectra and discovered 383 new sources. While the uncertainties provided in this study are mostly very small, some stars show very high uncertainties in surface gravity. Hence, we added 1859 stars to our sample that are members of Orion A and have an uncertainty in surface gravity smaller than 0.5.

Vioque et al. (2020) used a machine learning approach to find pre-main-sequence stars. We queried the TESS Input Catalogue (TIC) (Stassun et al. 2018) using the sample by Vioque et al. (2020) for entries that include values for the surface gravity and present new pre-main-sequence pulsators and candidates found in the TESS and CoRoT data to expand upon the literature sample. We describe our stellar evolution models and pulsation analysis in Sect. 5 and present our results in Sect. 6. Finally, we give our concluding remarks in Sect. 7.

2. Stellar sample

For our analysis, we searched the available literature for spectrophotometric surveys of young clusters and star-forming regions. Here, we describe the surveys used in this work and our selection process.

2.1. Pre-main-sequence and early ZAMS stars
effective temperature. A total of 705 stars have an entry for both and we added these to our sample.

Although the last two samples of Da Rio et al. (2016) and Vioque et al. (2020) provide spectroscopic surface gravities and effective temperatures, we assigned higher weights to the other surveys. For Da Rio et al. (2016), the reasoning is mainly based on the different wavelengths at which the spectra were obtained and the very small uncertainty overall (only a few Kelvin for a large subset of stars), which we interpret as formal and not astrophysical errors. For Vioque et al. (2020), the parameters come from different sources and, in part, no uncertainties are available. We include both samples in our discussion with smaller weights and focus more on the stars selected from the other samples.

2.2. Known pulsating pre-main-sequence stars

The pulsating pre-main-sequence stars and candidates used in this work include SPB, δ Scuti, γ Doradus, and δ Scuti – γ Doradus hybrids from different studies. In addition, we looked for pulsators among the stars in our sample of pre-main-sequence and early ZAMS stars in the TESS Data (see Sect. 3) and we go on to discuss previously unpublished pulsators found with CoRoT (see Sect. 4).

2.2.1. Slowly pulsating B stars

Gruber et al. (2012) reported the cases of GSC 00154-00785 and GSC 00154-01871 which are two probable members of the young open cluster NGC 2244. Zwintz et al. (2017a) performed a photometric study of young B stars in the young open cluster NGC 2264, resulting in the discovery of four early ZAMS SPB stars. Ten new slowly pulsating B stars were discovered by Fedurco et al. (2020). Two of them, HD 61712 and HD 36999 are potential pre-main-sequence SPB candidates. Ketzer et al. (2020) reported the case of 2MASS J16260931-2434121, a member of the ρ-Ophiuchus star-forming region embedded in the Upper Scorpius region. Given the young age of ρ-Ophiuchus, 2MASS J16260931-2434121 is a prime candidate for a pre-main-sequence SPB star. Labadie-Bartz et al. (2020) report g-mode frequency groups for HD 114981, a star in the sample by Alecian et al. (2013), which makes it another potential pre-main-sequence SPB star. In total, our literature sample includes ten pre-main-sequence or early ZAMS SPB stars and candidates.

2.2.2. δ Scuti stars

Zwintz et al. (2014) showed the existence of a relationship between pulsation properties and evolutionary stage for pre-main-sequence δ Scuti stars. Their work includes 34 δ Scuti stars in their pre-main-sequence to early ZAMS evolutionary phases. Additionally, Mellon et al. (2019) reported the discovery of δ Scuti-type pulsation in HD 156623, Barceló Forcada et al. (2020) proposed a scaling relation for δ Scuti stars. Their sample includes HD 287841 and HD 290764, two stars which are Herbig AeBe stars according to Fairlamb et al. (2015). Recently, Murphy et al. (2021) reported the case of HD 139614, a pre-main-sequence candidate δ Scuti star. Murphy et al. (2020) reported p-mode oscillations in HD 68695 and classify it as a λ Bootis star. HD 68695 is included in the sample by Fairlamb et al. (2015) and added to our sample as pre-main-sequence δ Scuti candidate. Our literature sample of pre-main-sequence δ Scuti stars comprises a total of 39 stars.

2.2.3. γ Doradus stars and δ Scuti γ Doradus hybrids

Only two pre-main-sequence γ Doradus stars with known spectroscopic parameters are known from the literature. These are Cl* NGC 2264 V AS 20 and Cl* NGC 2264 V AS 87 discovered in CoRoT data by Zwintz et al. (2013). Ripepi et al. (2011) reported the only known δ Scuti γ Doradus hybrid, CoRoT 102699796.

2.3. Literature sample

The literature sample for this study is shown in Fig. 1. Furthermore, Fig. 1 includes newly discovered pre-main-sequence pulsators and candidates; we discuss these in Sects. 3 and 4. Typical uncertainties have been calculated by taking the median plus the standard deviation of the uncertainties for all stars from a given source.

3. TESS observations

3.1. The TESS mission

The TESS satellite (Ricker et al. 2015) was launched on 18 April 2018 from Cape Canaveral on a SpaceX Falcon 9 Rocket, into a never-before-used lunar-resonant orbit known as P/2 (Gangestad et al. 2013). TESS carries four cameras, each with a 24 × 24 degree field of view used to survey almost the entire sky within two years in the primary mission. The research goal of the MIT-led NASA TESS mission is the discovery of transiting exoplanets. However, the high-quality light curves provide many more research opportunities, in the field of asteroseismology,

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1 Most of the stars in the study by Alecian et al. (2013) do not have uncertainties for the surface gravity. In such a case, we adopted an uncertainty of 0.5 dex. The typical error for these stars does not include the added standard deviation for the values of surface gravities.
for instance. More information about the TESS mission can be found in Ricker et al. (2015).

### 3.2. Data reduction and analysis

Multiple stars in our sample of pre-main-sequence and early ZAMS stars have been observed by the TESS mission. For most of these stars, no short-cadence data are available. In such a case, we use the python package `lightkurve` (Lightkurve Collaboration 2018) to obtain the full frame images (FFIs) and extract the TESS long cadence light curve. The latter is either a corrected light curve, where the scattered light is removed with the `smurfs` package (Müllner 2020) to perform a Fourier analysis in an iterative process. At the start of every iteration, it calculates a Lomb-Scargle periodogram (Lomb 1976; Scargle 1982) to detect the frequency and the amplitude of the highest peak. Here, `smurfs` uses these and a phase of 0.5 as initial values to perform a single sine fit to the residual light curve. The corresponding sine is subtracted from the residuals for the future iterations. We consider frequencies to be significant if their amplitudes exceed four times the local noise level ($S/N > 4$) (Breger et al. 1993; Kuschnig et al. 1997) and this procedure is continued until five consecutive frequencies are insignificant. With the exception of the data downlink gap at the beginning of each orbit, TESS light curves closely approach evenly spaced time series. This results in an almost vanishing spectral window (see Fig. A.1) that allows us to ignore possible alias frequencies.

Stars often appear in multiple systems such as binaries. Some of the stars discussed in the following are known binary stars, while other stars might be unknown multiple systems. Depending on stellar and orbital parameters, binarity may influence the frequencies extracted from Fourier analysis. This can range from the addition of frequency peaks at multiples of the orbital frequencies (ellipsing binaries, heartbeat stars, etc.) to the splitting of self driven pulsation modes into multiplets by differential rotation (Steindl et al. 2021). The first may, in some cases be misinterpreted as a signal of rotational variability, but is clearly distinguishable from a pulsation signal, in which the frequencies are not multiples of the orbital frequencies. Hence, the influence of binarity on the newly discovered pre-main-sequence pulsators (presented in the following) mostly affects the identification of the primary or secondary as the origin of the pulsation signal and has a minor influence on the extracted frequencies an the detection of pulsation itself.

We use TESS FFIs, TIC, and Gaia (Gaia Collaboration 2016) data to clarify the source of the variability. In total, six new SPB, six new δ Sct, and one new γ Doradus pulsators were identified in the TESS data of pre-main-sequence and early ZAMS stars, which we added to our sample. Their stellar properties are listed in Table 1.

### 3.3. Slowly pulsating B stars

**BD+65 1637** is a B3IV-Ve star (Aveni & Hunter 1972) observed in sectors 16, 17, 18, and 24. Short-cadence data are available for all of these sectors. BD+65 1637 is a member of the young open cluster NGC 7129 with an age smaller than 3 Myr (Straižys et al. 2014). Furthermore, Straižys et al. (2014) give an age of 0.27 Myr for BD+65 1637. We extracted 19 significant frequencies, mostly in the range between 3 and 5.5 d$^{-1}$, indicating g-mode pulsations. In addition, a few frequencies higher than 8 d$^{-1}$ are significant, also indicating p-mode pulsations. Given the young age of NGC 7129 and especially of BD+65 1637, the latter is an excellent candidate for classification as a pre-main-sequence SPB star. With $T_{\text{eff}} = 18000 ± 1000$ K and

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### Table 1. Stellar and pulsational properties of the newly discovered pulsators with TESS and CoRoT.

| Designation | TIC ID | Magnitude V | ST | $T_{\text{eff}}$ (K) | log g | Source | Type | Frequency range(s) (d$^{-1}$) |
|-------------|--------|-------------|----|----------------------|-------|--------|------|-------------------------------|
| HD 152872   | 247980805 | 9.07 | 8.84 | 650 ± 430          | 2.00  | A13    | SPB  | 3.9 – 55.8                     |
| HD 152799   | 247981153 | 8.74 | 8.67 | 675 ± 430          | 2.00  | A13    | SPB  | 3.9 – 55.8                     |
| HD 329271   | 247981406 | 10.65 | 10.51 | 690 ± 430         | 2.00  | A13    | SPB  | 3.9 – 55.8                     |
| HD 317861   | 102141335 | 9.83 | 9.52 | 685 ± 430          | 2.00  | A13    | SPB  | 3.9 – 55.8                     |
| HD 76534    | 30051402  | 7.5  | 8.07 | 650 ± 430          | 2.00  | A13    | SPB  | 3.9 – 55.8                     |
| HD 287823   | 459900291 | 9.74 | 9.58 | 650 ± 430          | 2.00  | A13    | SPB  | 3.9 – 55.8                     |
| HD 290500   | 50665450  | 11.04 | 10.75 | 670 ± 430         | 2.00  | A13    | SPB  | 3.9 – 55.8                     |
| 599 Ori     | 332912417 | 13.7 | 13.66 | 685 ± 430          | 2.00  | A13    | SPB  | 3.9 – 55.8                     |
| TYC 5851-2002-1 | 355320922 | 10.9 | 10.55 | 670 ± 430       | 2.00  | A13    | SPB  | 3.9 – 55.8                     |
| HD 144432   | 67671603  | 8.19 | 7.8 | 650 ± 430          | 2.00  | A13    | SPB  | 3.9 – 55.8                     |
| HD 135434A  | 207606851 | 7.76 | 7.71 | 650 ± 430          | 2.00  | A13    | SPB  | 3.9 – 55.8                     |
| HD 317859   | 102141942 | 9.52 | 9.04 | 650 ± 430          | 2.00  | A13    | SPB  | 3.9 – 55.8                     |
| CP* NGC 2264 VAS 196 | 231147340 | 10.07 | 10.80 | 685 ± 430       | 2.00  | A13    | SPB  | 3.9 – 55.8                     |
| CP* NGC 2264 VAS 219 | 231147743 | 12.09 | 11.85 | 670 ± 430       | 2.00  | A13    | SPB  | 3.9 – 55.8                     |
| CP* NGC 2264 VAS 230 | 231147556 | 12.37 | 11.66 | 670 ± 430       | 2.00  | A13    | SPB  | 3.9 – 55.8                     |

Notes. The column source refers to the stellar parameter and the shortcuts refer to the following articles: A13: Alecian et al. (2013), F15: Fairlamb et al. (2015), A18: Aidelman et al. (2018). Sources for the spectral types can be found in the main text.

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2 See the tutorials of `lightkurve` at [https://docs.lightkurve.org](https://docs.lightkurve.org)
\( \log(g) = 4.0 \pm 0.5 \) (Alecian et al. 2013), it was added as a young SPB star to our sample.

**HD 152822** is a B5/6IV star (Houk 1978) observed in sector 12. No short-cadence data are available for this star, hence, we used the light curve obtained using the RegressionCorrector. HD 152822 has a TESS magnitude of 8.844 and is listed as a double or multiple star in SIMBAD. Indeed, two stars with TESS magnitudes of 9.589 and 10.004, namely: TIC 1336947049 and TIC 1336947057, share nearly the same position. None of the two are listed in SIMBAD. As a consequence, we lack the possibility to further constrain this assumed multiple system. In the aperture we chose, there are four more stars with relevant magnitudes (we chose a cut-off Gaia magnitude of HD 152822 minus ~6). Three of them have an entry in SIMBAD, namely NGC 6250 7, NGC 6250 6, and NGC 6250 5, with their respective TESS magnitudes of 11.7078, 12.130, and 10.966. The last one, Gaia DR2 5963933729737076736, is by far the faintest of the four, with a Gaia magnitude of 14.541. We extracted eight significant frequencies, of which five are in the frequency range of 0.8 to 2.5 d\(^{-1}\) and an additional triplet around 4.8 d\(^{-1}\). These frequencies clearly indicate \( g \)-mode pulsations. Given the involved magnitudes and the amplitude of the extracted frequencies, it is most likely that the pulsations originate in one of the three stars assumed to build up the multiple system. Since the spectroscopic parameters of HD 152822 are consistent with SPB stars, we view HD 152822 as an SPB candidate with \( T_{\text{eff}} = 18236 \pm 625 \text{K} \) and \( \log(g) = 4.30 \pm 0.07 \) according to Aidelman et al. (2018). The FFI and chosen aperture are shown in Fig. A.4.

**HD 152799** is a B2/III star (Houk 1978) observed in sector 12. No short-cadence data are available for this star, hence, we used the light curve obtained using the RegressionCorrector. HD 152799 has a TESS magnitude of 8.674 and only one relevant star is in the chosen aperture, namely, Gaia DR2 5963932424051841536, with a TESS magnitude of 12.626. Three fainter stars are just outside the aperture to the north. We extracted five significant frequencies in the range from 0.7 to 4.5 d\(^{-1}\), clearly indicating \( g \)-modes. In addition, two frequencies in the same range fall just short of our significance criterion. Aidelman et al. (2018) reports \( T_{\text{eff}} = 22919 \pm 1577 \text{K} \) and \( \log(g) = 4.31 \pm 0.04 \), which is hotter and thus presumably more massive compared to known young SPB stars. Given that no comparably bright stars are directly in the aperture, we view HD 152799 as SPB star, but given its effective temperature, it is highly unlikely to be in its pre-main-sequence phase. However, more observations, preferably with better angular resolution, are needed to verify this classification and, hence, we added it as candidate to our sample. The FFI and chosen aperture are shown in Fig. A.5.

**HD 329271** is a B4V (Aidelman et al. 2018) star observed in sector 12. No short-cadence data are available for this star hence we use the light curve obtained using the RegressionCorrector. HD 329271 has a TESS magnitude of 10.515 and only one other relevant star is in the chosen aperture, namely, Gaia DR2 5963932252267675392, with a TESS magnitude of 14.083. We extracted two close frequencies at 2.473508 and 2.51648 d\(^{-1}\). The frequency range indicates \( g \)-mode pulsation. However, the first frequency is very close to F5 extracted for HD 152822. Depending on the chosen aperture and the size of FFI cutoff, this frequency can sometimes also be found for HD 152799. Given that the three stars lie close to each other, this signal might be of instrumental origin. Therefore, we view HD 329271 with \( T_{\text{eff}} = 18074 \pm 623 \text{K} \) and \( \log(g) = 4.26 \pm 0.06 \) (Aidelman et al. 2018) as a less reliable SPB candidate compared to the two other cases. The FFI and chosen aperture are shown in Fig. A.6.

**HD 317861** (CD-32 12908) is a B3Ve (Aidelman et al. 2018) star observed in sector 12. No short-cadence data are available for this star, hence, we used the light curve obtained using the RegressionCorrector. CD-32 12908 has a TESS magnitude of 9.516. Two other stars are in the chosen aperture, namely: NGC 6383 75 and Gaia DR2 4054593854958545536, with TESS magnitudes 12.283 and 14.798. We extract twelve significant frequencies mainly in the range around 1.2, 2.5, and 5.2 d\(^{-1}\) and one at around 7.3 d\(^{-1}\). The frequency list and light curve morphology strongly indicate \( g \)-mode pulsation. However, an additional frequency around 11.5 d\(^{-1}\) and some accessory signal in the amplitude spectrum suggest existence of possible \( p \)-modes. According to the TIC, NGC 6383 75 has \( T_{\text{eff}} = 7530\text{K} \) and \( \log(g) = 4.05796 \), in the range of \( \gamma \) Doradus stars. However, given the magnitude difference of the stars and the amplitude of the frequencies, we prefer the hypothesis that (at least the higher amplitude frequencies) originate from CD-32 12908. Additional observations, especially with better angular resolution is needed to verify any identification. We consider CD-32 12908 with \( T_{\text{eff}} = 20473 \pm 822 \text{K} \) and \( \log(g) = 4.23 \pm 0.09 \) (Aidelman et al. 2018) as an SPB candidate. The FFI and chosen aperture are shown in Fig. A.7.

**HD 76534** is a binary system where the primary is a B2Vn star (Houk 1978). The binary has been observed in sector 8 and 9. With a TESS magnitude of 8.07, the primary is significantly brighter than the secondary (which has a magnitude of 9.409). Short-cadence data are available for both sectors, hence, we downloaded the PDCSAP flux from the MAST portal. We extracted 16 significant frequencies, mostly around 2.5, 5, and 9 d\(^{-1}\). Two additional frequencies are just below our significance criterion. The light curve of HD 76534 hence clearly indicates \( g \)-mode pulsations. However it is unclear whether the primary or the secondary is the source of the variability. For the purposes of our study, we assumed that the primary with \( T_{\text{eff}} = 19000\pm500 \text{K} \) and \( \log(g) = 4.1 \pm 0.2 \) (Fairlamb et al. 2015) is a new SPB star candidate. Figure 2 shows the light curves and amplitude spectra of all SPB stars and candidates found in this work and the extracted frequencies are given in Table A.2.

### 3.4. \( \delta \) Scuti stars

Amplitude spectra calculated from light curves extracted from TESS FFIs suffer from a Nyquist limit of 24 d\(^{-1}\) (Murphy 2015). Real frequencies are reflected across the Nyquist frequency (Murphy 2012; Bell 2020). Given that pre-main-sequence \( \delta \) Scuti stars typically show oscillations below and above 24 d\(^{-1}\) (Zwintz et al. 2014), it is unclear whether the extracted frequencies are intrinsic to the star or Nyquist-aliases. However, the presence of the signal, independent of the intrinsic value, allows for the identification of the pulsation type. Figures 3 and 4 show the light curves and amplitude spectra of all six \( \delta \) Scuti stars and candidates extracted from FFIs found in this work and the extracted frequencies are given in Tables A.4 and A.5, respectively.

**HD 287823** is an A0 star (Vieira et al. 2003) observed in sector 6. No short-cadence data are available for this star, hence, we used the light curve obtained using the RegressionCorrector. We remove some long term variability using a Savitzky-Golay filter with a window length of 101, which removes intrinsic
frequencies below 1 d\(^{-1}\), but does not influence the \(p\)-mode frequencies. Most notably, this removes significant frequencies at 0.13334, 0.35863, and 0.32184 d\(^{-1}\). With \textit{Gaia} DR2 3234348869128541952, only one other star lies within the chosen aperture even though the TESS magnitude is quite high (14.344) compared to the magnitude of 9.579 for HD 287823. Three more stars lie in the vicinity, none of which are brighter than 12.08 magnitudes. Hence, we do not expect strong contamination from these sources. We extract eleven significant frequencies in the range of 16.1 to 23.75 d\(^{-1}\) (see Table A.4), clearly indicating \(p\)-mode pulsation. More frequencies above the Nyquist frequency (24 d\(^{-1}\)) might be expected from shorter cadence data. Given its classification as Herbig Ae/Be star, we view HD 287823 as a pre-main-sequence \(\delta\) Scuti star with \(T_{\text{eff}} = 8375 \pm 125\) K and \(\log(g) = 4.23 \pm 0.15\) (Fairlamb et al. 2015). The FFI and chosen aperture are shown in Fig. A.8.

HD 290500 is an A2 star (Vieira et al. 2003) observed in sector 6. No short-cadence data are available for this star, hence, we used the light curve obtained using the RegressionCorrector. We remove some long term variability using a Savitzky-Golay filter with a window length of 75, which removes intrinsic frequencies below 1 d\(^{-1}\) but does not influence the \(p\)-mode frequencies. Two stars lie just at the outer edge of the chosen aperture but HD 290500 outshines them by at least four magnitudes. We extracted 16 significant frequencies in the range of 17.6 to 23.76 d\(^{-1}\) (see Table A.4), clearly indicating \(p\)-mode pulsation. More frequencies above the Nyquist frequency (24 d\(^{-1}\)) might be expected from shorter cadence observations. Given its classification as a Herbig Ae/Be star, we view HD 290500 as a pre-main-sequence \(\delta\) Scuti star. With an effective temperature of 9500 \pm 500 K (Fairlamb et al. 2015), it appears to be very hot for a pre-main sequence \(\delta\) Scuti star. In comparison, Alecian et al. (2013) reported an effective temperature of 9000 \pm 500 K, indicating that it might actually be located at a lower effective temperature. Only a high-resolution, high S/N spectrum would provide a more reliable value in the future. A previous study performed by Díaz-Fraile et al. (2014) was inconclusive concerning the variability, but the TESS observations allow for a clear identification. In addition, the frequencies F12 and F18 seem to be a signal of rotational variability, indicating a surface rotation period of approximately 0.7 d. The FFI and chosen aperture are shown in Fig. A.9.

V599 Ori is as A8/9 star (Hsu et al. 2013) observed in sector 6. No short-cadence data are available for this star and the RegressionCorrector fails for this target. Hence, we use the BCSAP flux light curve. We remove some long term variability using a Savitzky-Golay filter with a window length of 75, which removes intrinsic frequencies below 1 d\(^{-1}\) but does not influence the \(p\)-mode frequencies. A dark star lies just outside the chosen aperture and should not lead to strong contamination. However, the pulsating naked eye star 49 Ori lies in the same region of the sky. Given its brightness, some contamination might be expected. We extracted seven significant frequencies in the range of 17.5 to 23.3 d\(^{-1}\) (see Table A.5), clearly indicating \(p\)-mode pulsation. More frequencies above the Nyquist frequency (24 d\(^{-1}\)) might be expected. Some additional frequencies might indicate \(g\)-mode pulsations as well. This makes V599 Ori a fascinating object to study, especially as the spectroscopic parameters by Fairlamb et al. (2015) with \(T_{\text{eff}} = 8000 \pm 250\) K and \(\log(g) = 3.72 \pm 0.13\) would indicate that the effective temperature is too high for \(g\)-modes. However, the influence of 49 Ori on the extracted light curve of V599 Ori warrants special attention. In addition, the fact that we are using a very simple background corrected aperture photometry does not enhance our trust in the extracted frequencies. A dedicated analysis as well as additional observations will be needed to properly classify this object. We view V599 Ori as \(\delta\) Scuti candidate. The FFI and chosen aperture are shown in Fig. A.10.

TYC 8581-2002-1 is an A5V star (Vieira et al. 2003) observed in sector 8, 9, and 10. No short-cadence data are available for this star, hence, we used the light curve obtained using the RegressionCorrector. Multiple stars lie in the vicinity of TYC 8581-2002-1; given that we have multiple sectors of FFI data, the stars that lie within the aperture vary slightly. TYC 8581-2002-1 has a TESS magnitude of 10.547, while a very nearby star, namely, \textit{Gaia} DR2 5302462513641062144, has a TESS magnitude of 10.954 and lies within the aperture in all sectors. \textit{Gaia} DR2 5302462346139414656 lies to the East of TYC 8581-2002-1 and is either just inside (in sector 10) or outside the aperture (in sectors 8 and 9). We extracted 13 significant frequencies in the range from 11.1 to 22.3 d\(^{-1}\) (see Table A.5), clearly indicating \(p\)-mode pulsation. More frequencies, above the Nyquist frequency (24 d\(^{-1}\)) might be expected. We find one additional frequency, possibly indicating a surface rotation period of approximately 0.57 d. The TIC reports an effective temperature of 7145 K for \textit{Gaia} DR2 5302462513641062144,
which is well within the range typical for δ Scuti-type pulsations. With the current observations, it is impossible to definitely attribute the pulsation signal to any of these stars and thus we chose TYC 8581-2002-1, with $T_{\text{eff}} = 9750 \pm 250$ K and $\log(g) = 4.0 \pm 0.1$ (Fairlamb et al. 2015) as a δ Scuti candidate. The FFI and chosen aperture for sector 10 are shown in Fig. A.11.

HD 144432 is an A9/F0V star (Houk 1982) observed in sector 12. No short-cadence data are available for this star, hence, we used the light curve obtained using the RegressionCorrector. We remove some long term variability using a Savitzky-Golay filter with a window length of 101, which removes intrinsic frequencies below 1 d$^{-1}$ but does not influence the $p$-mode frequencies. HD 144432 is a known multiple system (Müller et al. 2011) and given their analysis, we assume that HD 144432A is mainly responsible for the signal in the chosen aperture and, hence, also the variability. We extracted 12 significant frequencies in the range of 13.1 to 23.2 d$^{-1}$ (see Table A.4), clearly indicating $p$-mode pulsation. More frequencies above the Nyquist frequency (24 d$^{-1}$) might be revealed if short-cadence data were available. In addition, F1 seems to be a signal of rotational variability, indicating a surface rotation period of approximately 1.12 d. Since the spectroscopic parameters of the other members of this system are unknown, we identify HD 144432 with $T_{\text{eff}} = 7500 \pm 250$ K and $\log(g) = 4.05 \pm 0.17$ (Fairlamb et al. 2015) as δ Scuti candidate. The FFI and chosen aperture are shown in Fig. A.12.

HD 135344A is an A0V (Houk 1982) primary of a binary system observed in sector 11. Short-cadence observations are available for both the primary and secondary component. We remove strong long term variability using a Savitzky-Golay filter with a window length of 201, which removes intrinsic frequencies below 5 d$^{-1}$ but does not influence the $p$-mode frequencies. We extracted seven significant frequencies in the range of 60.5 to 80.9 d$^{-1}$ (see Table A.4), clearly indicating $p$-mode pulsation. Additional, albeit insignificant, signals in the amplitude spectrum are observed at frequencies in the range of 250 to 335 d$^{-1}$. Clearly, contamination from the secondary is expected in the light curve of the primary. However, the amplitude of the signal is evidently stronger in the light curve of HD 135344A and hence we identify it as δ Scuti candidate with $T_{\text{eff}} = 6750 \pm 250$ K and $\log(g) = 4$ (Alecian et al. 2013). Figure 3 shows the un-smoothed light curve and corresponding amplitude spectrum of HD 135344A. The pulsation signal around 80 d$^{-1}$ and the additional high frequency signal can clearly be seen.

### 3.5. γ Doradus stars

**HD 317859 (CD-32 12910)** is a F3V (Lloyd Evans 1978) star observed in sector 12. No short-cadence data are available for this star, hence, we use the light curve obtained using the RegressionCorrector. We remove some long term variability using a Savitzky-Golay filter with a window length of 601, which removes intrinsic frequencies below 0.2 d$^{-1}$. No other stars lie within the chosen aperture. We extracted eight significant frequencies around 1.2, 2.7, and 5.4 d$^{-1}$ (see Table A.3), clearly indicating $g$-mode pulsations. Lloyd Evans (1978) reported HD 317859 to be a member of the young open cluster NGC 6383 with an age of 4–5 Myr. At this estimated age, HD 317859 has a high probability to be a pre-main-sequence γ Doradus star with $T_{\text{eff}} = 7300 \pm 163$ K and $\log(g) = 4.34 \pm 0.01$ (Aidelman et al. 2018). However, a more reliable membership analysis is needed to verify this identification. We select HD 317859 as γ Doradus candidate. The FFI and chosen aperture are shown in Fig. A.13.

### 3.6. Other variable stars

We found additional variability in the TESS observations of CD-49 11096, PDS 344, HD 36382, HD 329379, HD 96042, HD 53367, and HD 152743 of different origins. We discuss these stars in more detail in Appendix A. Especially HD 329379 and HD 96042 should be interesting objects for follow up studies.

### 4. CoRoT observations

#### 4.1. The CoRoT mission

The CoRoT satellite (Auvergne et al. 2009) was launched on 2006, Dec. 27, from Baikonur onboard a Soyuz rocket into a polar, inertial circular orbit at an altitude of 896 km. CoRoT carried a telescope with 27 cm aperture and was able to observe stars inside two cones of 10° radius, one at RA = 06:50 and the other at RA = 18:50 using a filter bandwidth from 370 to 1000 nm. The main research goals of the CoRoT mission was the search for extrasolar planets and asteroseismology of main-sequence stars.

Three stars were originally discovered from CoRoT data to be candidate or bona fide pre-main-sequence γ Doradus or δ Scuti – γ Doradus pulsators. Their frequency content was confirmed using recent TESS observations. Table 1 lists their stellar properties.

#### 4.2. Observations, data reduction, and analysis

CoRoT observed two short run observations on the young open cluster NGC 2264: Short Run SRa01 was conducted in March 2008, providing a time base of observations of 23.4 days and Short Run SRa05 observed the field from December 2011 to January 2012 for about 39 days. For both observations, the complete cluster NGC 2264 was placed in one of the Exofield CCDs and data were taken for all stars in the accessible magnitude range from 10 to 16 mag in $R$.

For the present analysis, the reduced N2 data for all stars were extracted from the CoRoT data archive and the standard procedures for the reduction of CoRoT data were applied (see e.g., Zwintz et al. 2013). The CoRoT data reduction pipeline (Auvergne et al. 2009) flags those data points that were observed during the satellite’s passages over the South Atlantic Anomaly (SAA) and replaces them with linearly interpolated values. In
the present analysis, we omitted the linearly interpolated values, hence, we used only the data points obtained outside of the SAA. A detailed description of the CoRoT observations of NGC 2264 and the respective data reduction can be found, for example, in Zwintz et al. (2013).

We perform the Fourier analysis of CoRoT light curves in analogy to the TESS observations. Since CoRoT observes from a low-earth orbit, aliasing issues from the spectral window might be expected. Data reduction for the light curves presented in this study mostly removed these effects (see Fig. A.2 and Fig. A.3), such that the spectral window has no influence in the identification of pulsation type.

4.3. Pre-main-sequence γ Doradus stars in NGC 2264

Additionally, to the two previously reported pre-main-sequence γ Doradus stars (Zwintz et al. 2013), two further pre-main-sequence cluster members observed in the two CoRoT Short Runs on NGC 2264 showed g-mode type pulsations. Their light curves can be seen in Fig. 6. Only with high-resolution, high signal-to-noise spectra it was possible to clearly distinguish SPB from γ Doradus type pulsators and add an additional piece of information on the membership of the individual stars to NGC 2264. Appendix B describes the analysis of the spectroscopic data that led to the fundamental parameters used in the present study.

CI* NGC 2264 VAS 196 (CoID0223991870) is a F0/2 star (Karlsson 1972) that was observed by CoRoT in both Short Runs on NGC 2264 and by TESS in Sector 6 with a time base of 27 days. As the SRA05 data contain the longest continuous time base of ~39 days (Fig. 6), it also has the lowest noise level. Hence, we base our frequency analysis on this data set and compare to the shorter sets obtained by CoRoT in SRA01 and TESS in Sector 6. Nine frequencies were found to be significant in our analysis from the CoRoT SRA05 data (see Table B.1). The membership probability of CI* NGC 2264 VAS 196 to the cluster is reported to be 94% by Vasilevsksis et al. (1965). Hence, we added CI* NGC 2264 VAS 196 to our sample of pre-main-sequence γ Doradus pulsators.

CI* NGC 2264 VAS 219 (CoID0223997565) is an A7 star (Voroshilov et al. 1985) observed by CoRoT in both short runs on NGC 2264 and by TESS in Sector 6. The CoRoT data obtained during SRA05 has the longest uninterrupted time base of ~39 days (Fig. 6), hence yielding the lowest noise level. Consequently, we base our analysis on this data set and extract 24 significant g-mode frequencies in the range from 0.04 to 3.8 d−1; 15 of those can also be found in the CoRoT SRA01 data set and five in the TESS data (see Table B.2). We interpret the presence of several emission lines in the spectrum (see Fig. B.2) as an
Fig. 7. CoRoT observations of the newly discovered δ Scuti - γ Doradus hybrid candidate CI* NGC 2264 VAS 230. Left panel: light curve obtained in SRa01. The time is relative to start of the observations. Right panel: corresponding amplitude spectra derived from the light curve of SRa01.

indicator for stellar youth, and, hence, we added CI* NGC 2264 VAS 291 to our list of pre-main-sequence γ Doradus stars.

4.4. Pre-main-sequence δ Scuti - γ Doradus hybrid in NGC 2264

CI* NGC 2264 VAS 230 (ColID0223999101) is an A5 star (Voroshilov et al. 1985) that was observed by CoRoT in both short runs on NGC 2264 and by TESS in Sector 6. The CoRoT data obtained during SRa01 has the highest photometric precision, hence, it yields the lowest noise level despite the fact that SRa05 has the longer time base. Therefore, we base our analysis on the SRa01 data set and compare it to the SRa05 and TESS data. The light curve of SRa01 is shown in Fig. 7. We found five frequencies between 8.1 and 12 d$^{-1}$ that we identify as $p$-modes (F1 to F5 in Table B.3). The frequency at $\sim 14.8$ d$^{-1}$, which can easily be seen in Fig. 7, is related to the orbital frequency of the CoRoT satellite, and, hence, it was omitted in our analysis. Additionally, we detected four frequencies in the range from 2.1 to 3.3 d$^{-1}$ that might be $g$-modes (F6 to F9 in Table B.3). Hence, CI* NGC 2264 VAS 230 is a candidate pre-main-sequence δ Scuti - γ Doradus hybrid pulsator.

5. Stellar models

5.1. Stellar evolution models

The stellar evolution models in this work are calculated with version v-12778 of Modules for Experiments in Stellar Astrophysics (MESA, Paxton et al. 2011, 2013, 2015, 2018, 2019), which is a software instrument that solves the fully coupled physics (MESA, version v-12778 of Modules for Experiments in Stellar Astrophysics), which is a software instrument that solves the fully coupled physics (MESA, version v-12778 of Modules for Experiments in Stellar Astrophysics) to implement extensions of the otherwise very diverse code. We made use of this run_star_extras.f file to implement extensions to MESA as discussed in Sect. 5.1.3.

5.1.1. Input physics and chemical composition

For our models, we used the OPAL opacity tables (Seaton 2005) and the standard MESA equation of state (Paxton et al. 2011). We ignored the stellar rotation and magnetic fields. We used the mixing length description of convection developed by Cox & Giuli (1968) together with the Ledoux criterion and the description of convective premixing developed by Paxton et al. (2018) while not allowing for semi-convective. We used different values for the mixing length, $\alpha_{MLT}$, and employ exponential overshooting with $f = 0.01$ and $f_0 = 0.005$ at the top and $f = 0.005$ and $f_0 = 0.0025$ at the bottom of any convective zone.

The initial composition is subject to change in the models we calculate. Our standard model has an initial 1 H abundance of $X_H = 1 - X_{He} - X_{H2} - Z$, where $X_{He} = 85$ ppm, $X_{H2} = 0.224+2Z-X_{He}$, and an initial metallicity of $Z = 0.014$, according to the solar metallicity of Asplund et al. (2009). The mass fractions of metals are taken according to Asplund et al. (2009) updated based on Nieva & Przybilla (2012) and Przybilla et al. (2013).

5.1.2. Initial models

For the initial models of our calculations, we follow the description of Kunitomo et al. (2017), who followed the works of Stahler et al. (1980) and Hosokawa et al. (2011). In this approach, the initial mass and radius of a protostellar seed are set to 0.01 $M_\odot$ and 1.5 $R_\odot$, respectively. That is they correspond to slightly evolved protostars from stellar cores (Kunitomo et al. 2017) and they possess a high value for the initial entropy of the star (Baraffe et al. 2012). We refer to Kunitomo et al. (2017) for more details of the initial model and the influence of different initial values on the models.

5.1.3. Treatment of accretion

We follow the description of Baraffe et al. (2009) to model the influence of accretion in a one-dimensional stellar model. Hence, we adopted similar simplifications as Hartmann et al. (1997) and Siess et al. (1997). In this picture, the accretion onto the proto-star proceeds non-spherically. Thus, the object is free to radiate its energy over most of the photosphere (Hartmann et al. 1997). The accretion of material from the surrounding cloud introduces gravitational energy per unit of accreted mass, $-GM/R$, as well as internal energy, $+\epsilon GM/R$, to the system, leading to an energy rate of:

$$\frac{dE_{acc}}{dt} = (\epsilon - 1) \frac{GM}{R}.$$  

Here, $G$ is the gravitational constant, $M$ and $R$ are the mass and radius of the star in solar units, and $M$ is the accretion rate in solar masses per year. The value $\epsilon$ describes the geometry of the accretion process. Accretion from gravitationally bound material is described by $\epsilon \leq 1$, while $\epsilon \leq 0.5$ describes the accretion from a thin disk at the object’s equator (Hartmann et al. 1997; Baraffe et al. 2009). In this study, we followed the approaches of prior studies (e.g., Baraffe et al. 2009; Jensen & Haugbølle 2018) and chose $\epsilon = 0.5$.

The energy of the accreted material is either added to the star $(L_{add})$ or radiated away as accretion luminosity $(L_{acc})$.

The amount of each is controlled by a factor $\beta$, leading to:

$$L_{add} = \beta \epsilon \frac{GM}{R},$$  

and

$$L_{acc} = (1 - \beta) \epsilon \frac{GM}{R}.$$  

The case of $\beta = 0$ corresponds to cold accretion where all of the energy is radiated away, while $0 < \beta \leq 1$ corresponds to hot accretion.

3 Our MESA and GYRE input files are publicly available at https://zenodo.org/record/5115510.
accretion. However, \( \beta \) is expected to vary with accretion rate: a higher accretion rate corresponds to higher values of \( \beta \) (see e.g., Baraffe et al. 2012; Vorobyov et al. 2017; Jensen & Haubois 2018; Elbakyan et al. 2019, and references therein). In this study, we use a fixed accretion rate. Therefore, \( \beta \) is fixed to values in the range 0–0.5.

The energy added to the star is injected as extra heat. However, it is unclear how this extra heat is distributed inside the star. Descriptions vary from uniform distribution (e.g., Baraffe & Chabrier 2010) to heat injection only in the outer zones with a step function (Jensen & Haubois 2018). In this study, we follow the linear distribution of Kunitomo et al. (2017). Hence, the heat is distributed only in an outer region of fractional mass \( M_{\text{outer}} \) and increases linearly with the mass coordinate \( m \) according to:

\[
l_{\text{extra}} = \frac{l_{\text{shell}}}{M} \max \left(0, \frac{2}{M_{\text{outer}}} - \frac{m}{M} - 1 + M_{\text{outer}} \right).
\]

In this study, we vary \( M_{\text{outer}} \) in the range of 0.025–0.5.

The rate of accretion is most likely unique to any star-disk system. Numerical hydrodynamics simulations of such systems show that the accretion indeed varies substantially on a case-by-case level (Vorobyov & Basu 2010, 2015; Vorobyov et al. 2021). Such episodic accretion has been modelled with one-dimensional stellar evolution codes with assumed accretion rates (e.g., Baraffe et al. 2009, 2012; Baraffe & Chabrier 2010) as well as accretion rates stemming from such simulations (e.g., Vorobyov et al. 2017; Jensen & Haubois 2018; Elbakyan et al. 2019). However, this is computationally expensive and complicates the calculations of controlled stellar grids. Hence, we chose a constant accretion rate for this study.

Accreting evolutionary tracks are calculated until the central hydrogen abundance has dropped by 0.001 compared to the initial value. During the evolution of the accreting protostellar seed, we use MESA models at specific masses. These are saved once the mass of the accreting evolution is 0.001 \( \odot \) below the mass wanted at the ZAMS. A different MESA run then reads in these models to calculate the subsequent pre-main-sequence (post-accretion) evolution towards the ZAMS. At the start of this subsequent evolution, we continuously lower the accretion rate over a time of \( t_{\text{acc}} = 0.003/M \) for 500 equal timesteps according to:

\[
M(t_i) = M \left(1 - \frac{t_i - t_0}{t_{\text{acc}}} \right)^2,
\]

where, \( t_i \) is the star age at timestep \( i \) and \( M \) is the constant accretion of the protostellar evolution. Currently, we do not have a good understanding of the processes that lead to a halt in stellar accretion. As a consequence, we are unable to choose the accretion rate towards the end of the accretion process in a fully physically motivated sense. It is often a convenient choice to abruptly stop the mass accretion rate once the desired stellar mass is reached (see e.g., Kunitomo et al. 2017), while other approaches often assume an exponential drop over a few million years (see e.g., Elbakyan et al. 2019). As our approach needs to be applicable for both low and intermediate mass stars with vastly different time scales of stellar evolution, we choose a short timescale to decrease the accretion rate and allow the stellar model to relax to the non-accreting setup this way. This sharp termination of the accretion may be caused by photoevaporative winds creating holes in the inner disk regions and effectively cutting out the outer disk mass reservoir (Owen et al. 2011, 2012).

5.1.4. Atmospheric boundary condition

For the calculation of theoretical pulsation spectra, it is a necessity to build the atmosphere from a temperature-opacity (\( T-\tau \)) relation. We initially followed the work of Amard et al. (2019) and use the \( T-\tau \) relation described by Krishna Swamy (1966), with varying opacities, but we also calculated models using the relation by Eddington (1926). However, the use of OPAL opacity tables (Seaton 2005) lead to convergence problems for low-mass stars. Therefore, the initial models were constructed using \( \tau_{100} \) tables (Paxton et al. 2011) based on model atmospheres by Castelli et al. (2003) and Allard et al. (2001). For a solution of these convergence problems, we furthermore relax the error tolerance of the integration routine at the start of the evolution.

5.1.5. Shortcomings of our accreting models

Starting from a small protostellar seed of 0.01 \( \odot \) poses a problem to MESA that manifests itself in convergence issues. Hence, our evolutionary calculations require multiple retries and back-ups as the solver runs into problems. In addition, we are not able to perform a convergence study due to problems arising from smaller time steps and more zones. A typical protostellar evolution takes around \( \sim 9000 \) time steps, while the amount of zones rises from \( \sim 3000 \) in the initial model to \( \sim 9000 \) at the end of the evolution.

We were unable to produce accreting evolutionary tracks for any choice of input physics and we further discuss this aspect for the accretion rate. High accretion rates onto our 0.01 \( \odot \) starting model will not converge using a \( T-\tau \) atmosphere. However, starting from higher mass seeds allows us to explore accretion rates up to \( 10^{-2} M_\odot \) yr\(^{-1} \) for integrated atmospheric boundary conditions. Low accretion rates pose a different challenge. In this case, the calculation of the atmospheric boundary conditions fails due to problems with the opacity tables and the equation of state. This might be overcome by using \( \tau_{100} \) tables at the start of the evolution, and jumping to the \( T-\tau \) once a higher mass is reached (i.e., 0.04 \( M_\odot \)). While the influence of this approach on the accreting evolutionary track on the Hertzsprung-Russel or Kiel diagram is marginal, it influences seismic properties and, hence, is not an option for this study. However, we use the \( \tau_{100} \) tables to show results with different values of accretion rate. A different solution would be the use of different opacity tables at lower temperatures such as tables based on Freedman et al. (2008). However, we prefer the other opacity tables especially for the calculation of higher mass stars and thus decline this option.

In a similar manner, other input physics lead to convergence issues. These include, for example, very low values of \( \beta \), \( M_{\text{outer}} \) and the mixing length.

Emphasis has to lie on the physical interpretation of the evolutionary models calculated in this work. As discussed in Sect. 5.1.3, using a constant accretion rate is most probably not physical. Overall, we have not aimed to model individual stellar parameters but, rather, we find an envelope to contain the combined stellar parameters of our sample.

In addition, multiple assumptions have been made concerning the treatment of accretion. Currently, we miss the full physical description of how the energy of the accreted material is deposited inside the star. We expect that different descriptions will influence the outcome of our calculations to some degree.

5.2. Stellar pulsations

We used version 5.2 of the stellar oscillation code GYRE (Townsend & Teitler 2013; Townsend et al. 2018) to calculate
non-adiabatic pulsations of our stellar models. We refer to the above mentioned instrument papers for details on the numerical methods.

We calculated the dipole modes (i.e., harmonic degree \( l = 1 \)), with an azimuthal order of \( m = 0 \) for \( g \)-modes in the range \( n = -1, \ldots, -50 \) and \( p \)-modes in the range \( n = 1, \ldots, 50 \). These have to be calculated separately as they call for different frequency scan parameters; that is, we used frequency points distributed uniformly in inverse frequency for \( g \)-modes and distributed uniformly in frequency for \( p \)-modes. We look for frequencies in the range \( 0.05-10 \) d\(^{-1} \) for \( g \)-modes and \( 2-100 \) d\(^{-1} \) for \( p \)-modes. We chose regularity-enforcing inner boundary conditions and outer boundary conditions according to the formulation from Dziembowski (1971).

The time dependence of perturbations is assumed to be proportional to \( \exp(-i\omega t) \), where \( t \) is the time, \( i \) the imaginary unit, and \( \omega \) the eigenfrequency. In non-adiabatic calculations, \( \sigma \) is imaginary. Hence, the real part \( \sigma_R \) is associated with the period of oscillation

\[
\Pi = \frac{2\pi}{\sigma_R}
\]

and the imaginary part \( \sigma_I \) is associated with the growth rate

\[
\tau = \frac{1}{\omega_I}.
\]

Given an eigenmode, the sign of the growth decides whether the mode is excited (\( \tau > 0 \)) or stable (\( \tau < 0 \)). In other words, an eigenmode is unstable whenever the work, \( W \), of this mode is positive. The expression is given as:

\[
W = 4\pi \frac{\sigma_I}{\sigma_R}E,
\]

and describes the amount of energy change in the system performed by one cycle (Unno et al. 1989). Here, \( E \) is the total energy of oscillation. It is often convenient to explore the differential work \( dW/dx \) such that

\[
W = \int_0^1 \frac{dW}{dx} dx,
\]

where \( x \) is \( r/R \) is the coordinate of fractional radius. Hence, the differential work describes the driving and damping throughout the star. The normalised growth rate of:

\[
\eta = \int_0^1 \frac{dW}{dx} dx / \int_0^1 |dw/dx| dx,
\]

as proposed by Stellingwerf (1978), gives viable hints at the power of the driving. For \( \eta = 1 \), the entire stellar envelope contributes to the driving of the oscillation, while the envelope is entirely damping for \( \eta = -1 \). Typical values for excited modes in main-sequence SBP stars are values up to \( \sim 0.3 \) (see e.g., Townsend et al. 2018).

The description of convection is a known problem for one-dimensional stellar evolution codes (see e.g., Aerts 2021). The mixing length theory, first proposed by Böhm-Vitense (1958), uses averages of equations over lengths exceeding the typical travel length of convective motions (Aerts 2021). Hence, this description misses the time-dependence of stellar convection. As a consequence, we are missing the influence of time dependent convection on the pulsation properties. Dupret et al. (2005) showed that this time dependence is needed to produce the red edge of the \( p \)-mode instability strip. Similarly, this influences the obtained growth rates for \( \gamma \) Doradus stars. GYRE allows us to freeze convective heating altogether (case 1 of Pesnell 1990) or freeze the Lagrangian perturbation of convective luminosity (case 4 of Pesnell 1990). We explore the effect of choice in our results. Similarly, the linear nature of the pulsation equation prevents accurate calculation of the red edge of the pre-main-sequence \( p \)-mode instability strip as has been shown by Marconi & Palla (1998). The inclusion of non-linear effects and time-dependent convection for pre-main-sequence stars will be the subject of future works.

6. Results

Before calculating instability regions for the subsequent pre-main-sequence evolution, it is important to try and constrain the input physics for the accreting protostellar evolutionary track (see Sect. 5.1.3). We aim to find a set of input physics that results in an envelope (between the accreting evolutionary track and the ZAMS) that includes most pre-main-sequence stars in our sample. We find that the best values are given by an accretion rate of \( 5 \times 10^{-6} \) \( M_\odot \) yr\(^{-1} \) and \( \beta = 0.1 \). Additional parameters are only constrained marginally, as described in detail in Sects. 6.2 and 6.3.

The resulting instability strips provide constraints for the atmospheric boundary conditions of pre-main-sequence stars. We find that the Krishna-Swamy atmosphere does not reproduce the observed spectroscopic parameters for pre-main-sequence \( \delta \) Scuti stars while the Eddington-Grey atmosphere works successfully (see Sects. 6.4 and 6.5).

6.1. Stellar models from accreting protostars

The evolution of a star beyond the main sequence is primarily controlled by the stellar mass at which it arrives at the ZAMS. However, the evolution prior to the main sequence is inherently dependent on how the stellar model acquires the said mass. The classical pre-main-sequence evolution assumes an (unrealistic) initial model that has already obtained the mass of the main-sequence star. In contrast, accreting evolutionary tracks start as small stellar seeds and obtain their final ZAMS mass by means of accretion. In this section, we briefly summarise the differences in the pre-main-sequence evolutionary tracks for two distinct models that will, at some point, arrive at the ZAMS with the same stellar mass.

Figure 8 compares the evolution of a one and a four solar mass model for both, a classical pre-main-sequence evolution and the evolution from an accreting protostar. The initial accreting evolutionary track for both masses is the same for the latter (black lines in Fig. 8) since they both originate from the same stellar seed. From the evolution of the radius, it is evident that these models never reach the huge radii of the classical initial models. Once they have reached their final mass, they leave the accreting evolutionary track and continue their subsequent evolution towards the ZAMS. At this time, the position in the Kiel and Hertzsprung-Russel diagram of the one solar mass model is already similar to the classical model, while the stellar parameter of the four solar mass models converge only later.

Figure 8 also illustrates the internal structure of the stellar models. We searched for the \( MESA \) timestep where the surface gravity of the classical evolution models reaches the value of the models from accreting protostars after their accretion has stopped (black and blue dots in the top panels of Fig. 8). The models from accreting protostars show a temperature inversion
between the radiative core and the convective outer regions in the high density region towards the centre of the star. This is due to the heating of the stellar photospheric luminosity. Bottom left panel: time evolution of the stellar radius. Bottom right: temperature – density (cgs units) profiles of selected models which are marked with a circle in the Kiel and Hertzsprung-Russel diagrams.

6.2. Enveloping our stellar sample

We have calculated multiple accreting evolutionary tracks for different choices of input physics. The constraints from spectroscopic parameters of our sample are sufficient to limit some free parameters of the accretion picture we adopted (see Sect. 5.1.3).

We have chosen the following input physics as our standard model: an accretion rate of $M = 5 \times 10^{-6} M_{\odot} \text{yr}^{-1}$, fractional mass of the outer region $M_{\text{outer}} = 0.1$, mixing length parameter $\alpha_{\text{MLT}} = 1.8$, and factor $\beta = 0.1$ with Krishna-Swamy atmospheres and initial Deuterium abundance of 20 ppm. The accreting evolutionary track of this standard model is shown in Fig. 9, together with the resulting pre-main-sequence tracks and classical pre-main-sequence evolution. The accreting evolutionary track, together with the ZAMS, beautifully envelopes our stellar sample for lower temperatures and explains the 'missing' stars in the area between $\log(T_{\text{eff}}) = 3.6 - 3.8$ and $\log(g) = 3.2 - 3.75$.

However, this model does not envelop our complete stellar sample. Most notably, it reaches the ZAMS at approximately $6 M_{\odot}$ and cuts out multiple stars with effective temperatures higher than 15,000 K. This is not surprising since higher effective temperatures correspond to higher stellar mass. This in turn leads to shorter evolutionary timescales. Stars with O spectral types only have pre-main-sequence lifetimes of tens to hundreds of thousand years according to classical evolution models, making it increasingly difficult to observe such stars in their pre-main-sequence phase. At this timescale, they might still be embedded in their birth cloud when the stellar core already burns hydrogen in equilibrium. Furthermore, our calculations do not include input physics that would put them within the envelope of our accreting evolutionary track without straying far away from well-fitting envelope for lower temperatures. Therefore, we believe that most of these stars have arrived on the main sequence, or are even already in the post-main-sequence phase of their evolution.

A few more stars do not lie within the region enveloped by our accreting model and the ZAMS. Some stars of the sample by Fairlamb et al. (2015) lie just above the accretion model. This might be attributed to multiple reasons. While they might be (similar to the hotter stars) in their post-main-sequence phases, this is less probable at the respective temperature. A more logical explanation might be that they undergo phases of strong accretion. As our model assumes constant accretion rates, departures from this accreting evolutionary track are expected due to episodic accretion (Elbakyan et al. 2019). Given the uncertainties of the spectroscopic parameters (see Fig. 1) it is also possible that some even lie within the envelope. A few low-temperature stars of the sample by Da Rio et al. (2016, shown as pink symbols in Fig. 9) seem to have surface gravities above three. We suspect that these are either red giant branch stars or statistical outliers.

Two stars need special attention. The first one, Z CMa is part of the sample by Fairlamb et al. (2015). With $T_{\text{eff}} = 8500 \pm 500$ and $\log(g) = 2.53 \pm 0.17$ it lies far off our accreting model. This star is a well known FU Orionis object (Hartmann & Kenyon 1996), meaning it undergoes very strong accretion, leading to high luminosities. This leads to heating of the stellar envelope and increase in stellar radius (Elbakyan et al. 2019). This explains that the surface gravity is very low and the star does not fit within our envelope. The second one, 2MASS 11110238-7613327 is part of the sample by Gutiérrez Albarrán et al. (2020) as a member of Cha I. With $T_{\text{eff}} = 5032 \pm 56$ and $\log(g) = 3.26 \pm 0.09$ it lies in the area of the Kiel diagram where the accreting evolutionary track takes a dip in surface gravity. There is no literature available for this star and the TESS light curve does not show any variability. At this stage, we are unable to explain the reason for the star’s location in the Kiel diagram and we strongly encourage follow-up observations.

The samples by Da Rio et al. (2016) and Vioque et al. (2020) show some stars below the ZAMS. These might be dwarfs, but their existence does not influence our results for the accreting models.

6.3. Constraining the input physics with spectroscopic parameters

We calculated models that differ from the standard model by one parameter at a time. From the discussion in Sect. 6.2 it is clear that a significant portion of the stars in our sample of pre-main-sequence and early ZAMS stars might be in later evolutionary stages even tough they are of comparably young age (several million years old) because of the short evolutionary timescales of high-mass stars. Without a distinction between these stars and
genuine pre-main-sequence stars, it is not convenient to define a likelihood or merit function and then statistically infer a best-fitting model. As discussed in Sect. 5.1.5, the accretion history is most probably unique for each individual star. Furthermore, more massive stars have most likely undergone an early accretion phase with higher mass accretion rates than their lower mass counterparts. Hence, we rely on a subjective choice of the models, whenever the difference in the track is big enough to do so, without investigating a two dimensional parameter space and hence ignoring possible degeneracy. While different combinations may yield similar results (e.g., higher mass accretion rate and lower $\beta$-value) the values for our standard model are chosen to reflect what is typically used in the literature. Estimates for the mass accretion rates for molecular clouds temperatures of $\sim$30 K lead to a mass accretion rate of $\sim$10$^{-5}$ $M_\odot$ yr$^{-1}$ (Kunitomo et al. 2017). As such, we are inclined to remain near these estimates, rather than stray from them. The results are shown in Fig. 10 and discussed in detail below.

### 6.3.1. Atmospheric boundary conditions

Panel a shows the influence of the choice of atmospheric boundary conditions. We find that this choice only marginally changes the position of the accreting evolutionary track and, hence, the observationally determined atmospheric parameters cannot be used to constrain them. At the same time, this allows us to use $\tau_{100}$ table atmospheres to calculate evolutionary tracks for those cases that would otherwise lead to strong convergence problems.

### 6.3.2. Mass accretion rate

Panel b shows the influence of the mass accretion rate. It is evident, that the lower accretion rates of $M = 10^{-6}$ and $10^{-7} M_\odot$ yr$^{-1}$ cut in our stellar sample. In these cases, a lot of stars would need to undergo phases of variable accretion rates to explain their positions above the respective accreting evolutionary tracks. For the very high mass accretion rates of $M = 10^{-3}$ and $10^{-4} M_\odot$ yr$^{-1}$, the tracks cut the ZAMS at significantly higher masses. This would lead to the O-type stars in our sample that would still remain within the area enveloped between the accreting evolutionary track and the ZAMS. For these accretion rates, the increase in stellar radius leads to lower surface gravities. As a consequence, these accreting evolutionary tracks fail to describe the location of lower mass stars at temperatures below 16 000 K. Finally, the location of the track with $M = 10^{-5} M_\odot$ yr$^{-1}$ is comparably close to the one with an accretion rate of $M = 5 \times 10^{-6} M_\odot$ yr$^{-1}$, which we adopted for our standard model. The comparison of these tracks in the region below 10 000 K shows that the track with an accretion rate of $M = 5 \times 10^{-6} M_\odot$ yr$^{-1}$ follows the observations more closely and is to be preferred in our analysis.

### 6.3.3. Fractional mass of heat injection

In the description of accretion adopted in this work, $M_{\text{outer}}$ controls the position up until the extra heat from the accreted material is injected. Hence, for higher $M_{\text{outer}}$, larger parts of the stars are being heated. Intuitively, one would expect the accreting material to be able to penetrate only the very outer parts of the star. Panel c shows the influence of different choices of $M_{\text{outer}}$ onto the accreting evolutionary tracks which is largely confined to very early stages. We find that the descriptions using $M_{\text{outer}} \geq 0.2$ may be the only ones that might be considered unphysical as they cannot explain a small part of the sample. Additionally we do not expect the accreted material to penetrate that far into the star. Lower values of $M_{\text{outer}}$ lead to marginal differences that cannot be constrained with our spectroscopic sample.

Fig. 9. Comparison of the accreting evolutionary tracks from protostars to the classical pre-main-sequence evolution. The thick black line shows our accreting standard model and the thin black line the pre-main-sequence models evolved from this accreting model. Red lines show classical pre-main-sequence tracks with the same masses at the ZAMS as the pre-main-sequence models from the accretion protostar. The ZAMS is shown as grey line. The grey shaded area at higher temperatures marks the position of (post-) main-sequence stars according to our interpretation. The colour code of the stars is the same as in Fig. 1.
Fig. 10. Influence of chosen input physics on the accreting evolutionary track: (a) Different atmospheric boundary conditions. (b) Different constant accretion rates. (c) Different regions of heat injection. (d) Different values for the mixing length. (e) Different values for \( \beta \), controlling the amount of energy injected into the star. (f) Different initial abundances of Deuterium. Our standard model is shown as black lines in all panels. Lines appended with an dagger in panels b and e are calculated using the \( \tau_{100} \) instead of Krishna-Swamy atmosphere. The colour code of the stars is the same as in Fig. 1.

6.3.4. Mixing length of convection

Panel d shows the influence of different mixing lengths. Mixing lengths below \( \leq 1.5 \) lead to convergence issues and are hence omitted from this study. The influence of the mixing length on the accreting evolutionary track is marginal and therefore we cannot employ our sample to constrain it. However, we can observe that higher mixing lengths tend to cut into the sample obtained from Vioque et al. (2020).

6.3.5. Fraction of injected energy from accreted material

Panel e shows the influence of the parameter \( \beta \) that controls how much of the energy of the accreted material is injected into the star or radiated away. The case of \( \beta = 0 \) corresponds to cold accretion and definitely fails to explain our sample as it cuts through it at very high surface gravities. The story is similar for the small values \( \beta = 0.01 \) and \( 0.05 \). Values higher than the value adopted by us give accretion evolutionary tracks that have overly low surface gravities for small effective temperatures.

6.3.6. Deuterium abundance

Panel e shows the influence of the mass fraction of Deuterium in the initial composition of the stellar seed and the accreted material. Given the description of accretion adopted for the standard model, the Deuterium abundance only marginally influences the accreting evolutionary track. Most notably, increasing the Deuterium abundance leads to a smaller surface gravity after Deuterium ignition at approximately \( \log T_{\text{eff}} = 3.6 \). Hence, we cannot constrain the Deuterium abundance with our stellar sample.

6.4. Exploring the instability regions for pre-main-sequence stars

The calculations performed in this paper include the growth rates for dipole modes across the Kiel diagram. Figure 11 shows the resulting instability strips as the area where any mode is unstable. We discuss the implications of these results, starting with the \( p \)-mode instability region (left panel in Fig. 11).

All \( p \)-mode pulsating pre-main-sequence \( \delta \) Scuti stars within our sample lie within the calculated instability region. As expected, the red edge of the instability region does not agree with the observational red edge as implied by our sample. The non-inclusion of time-dependent convection leads to unstable modes in stars with effective temperatures below 6500 K. The normalised growth rates indicate that the driving is very strong in this part of the instability region. Figure 12 shows that the high values for the normalised growth rate come with low values of actual work performed by one pulsation cycle. Furthermore, the change towards higher values for the work is abrupt, leading to a clear boundary in Fig. 11. The temperature region of this boundary overlaps with observed effective temperatures of pre-main-sequence \( \delta \) Scuti stars in our sample. Hence, we propose that we interpret only the hotter part (higher temperatures than the boundary) as the \( \delta \) Scuti instability region. The remaining temperature region is similar to the one obtained by Dupret et al. (2005) and, hence, the unstable modes towards lower temperatures can be attributed to missing stabilisation effects from convection.

For \( g \)-modes, we obtain three distinct instability regions with our calculations (right panel of Fig. 11). With the exception of GSC 00154-01871, all SPB stars and candidates from our sample (that fall within our pre-main-sequence tracks) also lie in the SPB instability region. GSC 00154-01871 is a spectroscopic binary and the real physical parameters of the pulsating
star may differ from the adopted ones. Handler (2011) obtained \( \log g = 4.4\pm0.2 \) and \( T_{\text{eff}} = 14300\pm600 \) in contrast to the adopted values from Gruber et al. (2012) which are \( \log(g) = 3.80\pm0.15 \) and \( T_{\text{eff}} = 13900\pm350 \). However, \( \log(g) \) is primarily obtained from the H\alpha line, which is strongly affected by the companion.

We conclude that the position of GSC 00154-01871 in our Kiel diagram is most likely not correct. Hence, all SPB stars with well-defined parameters lie within our calculated pre-main-sequence instability region.

Our results show that it is possible to obtain the \( \gamma \) Doradus instability region even without time-dependent convection. This can only be accomplished by employing case 4 of Pesnell (1990) in the calculations with GYRE. Furthermore, case 1 will return stable modes throughout this region of the Kiel diagram. Hence, we strongly recommend using the description of case 4 when calculating \( g \)-modes with GYRE. While the blue edge of our instability region is well defined, the red edge appears problematic. The models in small regions seem to host stable modes only. We tried to increase the resolution of GYRE’s spatial grid but without success. We chose to draw the border to include the low temperature region \( (3.7 < \log(T_{\text{eff}}) < 3.75) \) of this instability region as these are the early parts of the pre-main-sequence \( \gamma \) Doradus tracks. However, it is most likely that the instability in this region is due to the influence of accretion (see discussion below). The resulting instability region includes all \( \gamma \) Doradus stars and \( \gamma \) Doradus – \( \delta \) Scuti hybrids. Two \( \gamma \) Doradus candidates are just outside the instability region, which is not concerning given the uncertainties on their positions.

We find an additional instability region for \( \log(T_{\text{eff}}) < 3.7 \). We are currently not aware of any known pulsators in this region of \( K \)- and \( M \)-type stars. Pulsation in these types of stars is expected (Baran et al. 2011; Rodríguez-López et al. 2012, 2014) and multiple projects look for observational discoveries (see Rodríguez-López 2019, for a review). We looked for possible pulsations in the TESS observations of \( K \)- and \( M \)-type stars and we present our results in Sect. 6.7.

Table 2 compares the temperature ranges of our instability regions with the published instability regions of pre-main-sequence stars by Marconi & Palla (1998), Grigahcene et al. (2006), Bouabid et al. (2011), and Gruber et al. (2012). Besides...
the blue edge of the \( p \)-mode instability region, our calculations offer a fair agreement with these previous results. Our sample includes five pre-main-sequence \( \delta \) Scuti stars and two candidates with effective temperatures above the blue edge of Grigahcene et al. (2006) at temperatures up to 8400 K. Based on our sample, the observational blue edge for pre-main-sequence stars lies around 8900 K. In later evolutionary phases, \( \delta \) Scuti stars are observed up to effective temperatures of 10,000 K, but much less frequently (Murphy et al. 2019). Given the size of our current sample, it is impossible to decide whether the blue edge resulting from our calculations is supported by real stars. Only a future increase in the number of observed pre-main-sequence \( p \)-mode pulsators can put this hypothesis to the test.

6.5. Constraining the input physics with pre-main-sequence pulsators

We calculated instability regions for models with different atmospheres and mixing length parameters. In addition, we compare the obtained results with instability regions obtained from classical models. The results are discussed in the following.

6.5.1. Atmospheric boundary conditions

Figure 13 shows the \( p \)-mode instability region for Eddington-Gray and Krishna-Swamy atmospheres. Models calculated with Krishna-Swamy atmospheres have no excited modes in a region of the Kiel diagram populated with known pre-main-sequence \( \delta \) Scuti stars. In comparison, the observed \( \delta \) Scuti stars are fully embedded in the instability region resulting from models using Eddington Gray atmosphere. Hence, it is evident that Krishna-Swamy atmospheres are not suitable for the modelling of pre-main-sequence stars.

6.5.2. Mixing length of convection

We calculated instability regions for models with \( \alpha_{\text{MLT}} = 1.8, 2.0, 2.2 \) (see Figs. D.1 and D.2). Both, the \( p \)-mode and \( \gamma \) Doradus instability region are influenced by the choice of input physics. Given the uncertainties of the stellar parameters, we were not able to constrain the mixing length with pre-main-sequence pulsators. Since higher mixing lengths cut into the stellar sample of Vioque et al. (2020), we note that \( \alpha_{\text{MLT}} = 1.8 \) fits best.

6.5.3. Comparison to classical evolution

Figure D.3 shows the comparison between classical models and the models from accreting protostars. The \( p \)-mode instability region is very similar, with the exception that lower surface gravity is allowed due to different initial models.

For SPB stars, the early phases off the accreting evolutionary track is stable to \( g \)-modes. This is different to the classical pre-main-sequence tracks, which show an instability at this location. The \( \gamma \) Doradus instability region is located at similar positions in both calculations, but the borders look significantly different. For the classical models, unstable modes are located in a smaller temperature region, and especially for low temperatures \((3.7 \leq \log(T_{\text{eff}}) \leq 3.75)\), no modes are excited. Hence, we attribute the instability region at these low temperatures and the widening of the temperature range found in our models of accreting protostars to an effect related to the accretion history.

6.6. Instability of higher order modes

Long-time base observations obtained with space telescopes allow for the identification of successive radial orders (see e.g., Li et al. 2020, for \( \gamma \) Doradus stars observed with Kepler). To investigate the potential of performing similar analyses for pre-main-sequence stars, we performed our calculations so that radial orders up to \( n = \pm 50 \) were included. A distinction of the observed pre-main-sequence instability regions including the information of which radials orders are excited will create more constraints on the input physics once sufficient observations of pulsating pre-main-sequence stars are available. Here, we report our results for the instability regions of higher orders for both \( p \)- and \( g \)-modes.

Figure 14 shows order-dependent pre-main-sequence instability regions for \( p \)-modes. There are two separate regions with unstable modes of radial order \( \geq 15 \): region I at lower temperatures \((3.75 \leq \log(T_{\text{eff}}) \leq 3.85)\) and region II at hotter temperatures \((3.9 \leq \log(T_{\text{eff}}) \leq 4)\). The blue boundary of region I coincides with the red edge of the observed instability deduced from our sample of pre-main-sequence and early ZAMS stars. Region I is most likely introduced by missing stabilisation effects due to convection, and, hence most likely non-physical.

In comparison, region II matches the location of observed pre-main-sequence \( \delta \) Scuti stars and candidates in our sample. As such, there are multiple known pulsators that fall within this part of the Kiel diagram. We strongly encourage the search for more pre-main-sequence pulsators to further populate the \( p \)-mode instability region.

Figure 15 shows order-dependent instability regions for \( g \)-modes with even more distinct features. For SPB stars, the results indicate the modes with radial orders \( |n| \geq 25 \) are confined to lower surface gravity. Astonishingly, all of the observed pre-main-sequence and early ZAMS SPB stars and candidates with well defined spectroscopic parameters fall within the region

\[ 19 \, 200 \, \text{K} \quad 18 \, 700 \, \text{K} \]

Table 2. Comparison of the temperature regions to previously calculated pre-main-sequence instability strips.

| Type     | MP98  | G06   | B11  | G12  | This work |
|----------|-------|-------|------|------|-----------|
| Note     | Non-linear | Linear | Linear | Linear | Linear |
| Radial order | 1–3 | TDC \((a)\) | TDC \((a)\) | ? \((b)\) | \( \beta \) \((b)\) |
| \( \delta \) Sct | 6500– | 6450– | – | – | 6300 \((c)\) |
| \( \gamma \) Dor | – | – | 6550– | – | 5200– |
| \( \gamma \) Dor | – | – | 7400 K | – | 7650 K 

Notes. \((a)\) Time dependent convection, \((b)\) accretion from protostellar seed, \((c)\) assumed from results, \((d)\) the red edge of the \( p \)-mode instability region is taken to be the boundary to high normalised growth rates as discussed in the text. \((e)\) The difference at the red edge is an accretion effect for modes with low radial order only. For radial orders \( \geq 15 \), we obtain the temperature range 6450–7550 K.

References. MP98: Marconi & Pallà (1998), G06: Grigahcene et al. (2006), B11: Bouabid et al. (2011), G12: Gruber et al. (2012).
stars. Future observations of higher accuracy should be able to deduce whether this is a real physical or a modelling effect. Our results furthermore indicate a region with excited modes with orders $1 \leq |n| \leq 15$ just below the accreting evolutionary track shown as the red area in Fig. 15.

The instability region for M-type stars described in Sect. 6.4 includes higher order modes at very early evolutionary stages. As such, we would expect to be able to observe period spacings at very low frequencies for such stars.

6.7. 2MASS J11120327-7637034: a possible pulsating M-type young stellar object

2MASS J11120327-7637034 (also CHXR 84, Hn 16, TIC 454364154, etc.) is a M5.5 (Luhman 2004) type star and a member of the Chameleon I region with an estimated age of 2 Myr (Gutiérrez Albarrán et al. 2020). TESS observed 2MASS J11120327-7637034 (TESS magnitude 14.062) in sector 14. No short-cadence data are available for this star and hence we obtained the light curve from the FFIs using the RegressionCorrector. The FFIs are very crowded, but the chosen aperture includes only three more stars (Gaia DR2 5201302259854227968, Gaia DR2 5201302259855579778304, and Gaia DR2 5201302259855437072) with magnitudes (19.326, 19.346, and 20.108 mag) that are significantly lower than the magnitude of 2MASS J11120327-7637034 from which no contamination is expected. Multiple other stars lie in the vicinity of 2MASS J11120327-7637034; given their magnitude, they might contaminate the extracted light curve to some degree. The FFI and chosen aperture are shown in Fig. A.14.

We extracted five significant frequencies (see Table 3). We attribute the frequencies F3 and F5 to rotational signal from stellar spots. Flaherty et al. (2016) found evidence for cold spots for 2MASS J11120327-7637034 that is consistent with this attribution. We furthermore interpret the other three frequencies as possible pulsation frequencies. Figure 16 shows the light curve and amplitude spectra extracted from the TESS FFIs. We removed the rotation signal (top panel) and the suspected pulsation signal (middle panel) to obtain the residuals in the bottom panel.

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**Fig. 13.** $P$-mode instability strips for different atmospheres. The green shaded area shows the result for Eddington Gray atmosphere, while the blue shaded area shows the result for the Krishna-Swamy atmosphere. The colour code of the shown pulsators is the same as in Fig. 1.

**Fig. 14.** $P$-mode instability regions dependent on the excited orders. The black lines show the accreting evolutionary track (dashed) and the pre-main-sequence evolution from this models (thin). Different coloured areas show the regions where modes with radial orders higher than $n \geq 1, 5, 15, \text{and} 25$ are unstable. The colour code of the shown pulsators is the same as in Fig. 1.

**Fig. 15.** $G$-mode instability regions dependent on the excited orders. The black lines show the accreting evolutionary track (dashed) and the pre-main-sequence evolution from this models (thin). Different coloured areas show the regions where modes with radial orders higher than $|n| \geq 1, 5, 15, \text{and} 25$ are unstable. The colour code of the shown pulsators is the same as in Fig. 1.

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The results for the pre-main-sequence $\gamma$ Doradus instability region indicate that mostly low order modes are excited. However, in a small region around 6750 K, higher order modes are expected. Hence, the situation is similar to the case of SPB...
The amplitude spectrum of the residuals shows evidence for more variability, but no more significant frequencies could be extracted.

Gutiérrez Albarrán et al. (2020) reported an effective temperature of $3304 \pm 103$ K, which is higher than the temperature expected from the spectral type, that is, 3058 K (Luhman et al. 2003; Luhman 2004). We looked for models with temperatures in the range of the values adopted by Gutiérrez Albarrán et al. (2020) in our grid. While the grid is sparse in the corresponding region of the Kiel diagram, we find two models for which dipolar $g$-modes are excited that match F1, F2, and F4 within a fourth of the Rayleigh limit which is 0.009 d$^{-1}$. Figure 17 compares the excited frequencies in these models with the observations. The specifics of the two models are given in Table 4. The stellar mass is higher than estimates by Kirk & Myers (2011) and Lafrenière et al. (2008). Both used the temperature estimate by Luhman (2004) and hence some discrepancy is expected. Feigelson & Lawson (2004) estimated the age of 2MASS J11120327-7637034 to be 1 Myr. This estimate of course relies on models that are not originating from accreting stellar seeds and hence this discrepancy is also expected.

Given the relatively poor observations at hand, it is clear that no full asteroseismic modelling can be done. However, it is promising that even such a sparse grid includes two models that fit the observed frequencies. A closer look at the amplitude spectrum in Fig. 17 shows an additional signal at around 0.8 d$^{-1}$ and 2.6 d$^{-1}$, where both models predict excited frequencies (radial orders $-1$ and $-3$), but the observational amplitudes are not significant. 2MASS J11120327-7637034 will be observed again in TESS sectors 38 and 39. With additional data, it might be possible to further constrain whether the variability originates from accreting stellar seeds or any other star in the vicinity and what its origin is. A longer baseline should also give better estimates for the observed frequencies and produce better constraints for modelling. We plan on re-evaluating the status of

### Table 4. Frequencies and stellar parameters for the models describing the observed frequencies of 2MASS J11120327-7637034.

| Parameter | Observed | Model A | Model B |
|-----------|----------|--------|--------|
| F1 (d$^{-1}$) | 1.27260(2) | 1.26706 | 1.27699 |
| Radial order | $-2$ | $-2$ | $-2$ |
| F2 (d$^{-1}$) | 0.19716(4) | 0.205598 | 0.190394 |
| Radial order | $-9$ | $-10$ | $-10$ |
| F4 (d$^{-1}$) | 0.24018(6) | 0.234298 | 0.243129 |
| Radial order | $-8$ | $-8$ | $-8$ |
| $T_{\text{eff}}$ (K) | 3304(103) | 3317.3 | 3368.7 |
| log($g$) | 3.299 | 3.289 | 3.289 |
| Radius ($R_\odot$) | $1.484$ | 1.592 | 1.592 |
| Mass ($M_\odot$) | 0.137$^a$, 0.15$^c$ | 0.16 | 0.18 |
| Age (Myr) | $1^d$ | 0.176 | 0.160 |

References: $^a$Gutiérrez Albarrán et al. (2020), $^b$Kirk & Myers (2011), $^c$Lafrenière et al. (2008), $^d$Feigelson & Lawson (2004)
presented light curves and pulsation spectra of new pre-main-
sequence stars, modelled using the MESA code. We then gathered a spectroscopic sample of pre-main-sequence and early ZAMS stars and constrained the input physics of accretion to obtain an envelope for these stars in a constant accretion scenario. This can be considered as a first step towards more realistic scenarios provided by episodic accretion rates either obtained from numerical hydrodynamics simulations or other more sophisticated approaches than this constant accretion scenario. While this effort was able to restrict the constant accretion rate and the fraction of injected heat from accreted material, other free parameters (i.e., the atmospheric boundary conditions, \(\alpha_{\text{MLT}}\), fractional mass of heat injection, and initial Deuterium abundance) cannot be constrained. The resulting accreting evolutionary track presents a good envelope to the stellar sample even though not all stars in the latter end up being interpreted as pre-main-sequence stars. However, besides one star, namely, 2MASS 11110238-7613327, we discuss the reason for its not fitting within the envelope; and we find that it is not of great concern. Not much is known about this constant accretion scenario. The resulting pulsation regions follow the position of the observed pulsators, with few exceptions. The \(p\)-mode instability region indicates unstable modes in low temperature regions, where no pulsating star is known. We attributed this to missing stabilisation effects from stellar convection, as our models do not include time dependent treatment of convection. A closer inspection of the results shows that the pulsation modes in the corresponding models have high normalised growth rates but the work performed by one pulsation cycle is almost vanishing. Furthermore, there is a clear border in normalised growth rate that coincides with the observed red edge of the pre-main-sequence instability region deduced from our sample of pre-main-sequence and early ZAMS stars. We hence propose to interpret only the part leading up to the hotter regions of this boundary as the pre-main-sequence \(p\)-mode instability region. Both the pre-main-sequence SPB and \(\gamma\) Doradus instability regions explain the observed pulsators. We have shown that is essential to use the description of case 4 of Pesnell (1990) when calculating the pulsation spectra of pre-main-sequence \(\gamma\) Doradus stars with GYRE.

While the instability regions obtained by our calculations are not able to constrain the mixing length, we have shown that Krishna-Swamy atmospheres are not able to produce the unstable \(p\)-modes in populated regions of the Kiel diagram. Hence, Eddington Gray atmospheres are to be preferred.

In addition, we discussed the instability of pre-main-sequence stars depending on the radial order of unstable modes. Future observations, with baselines long enough to identify \(g\)-mode period spacings, will allow for the testing of these obtained instability regions and, as such, provide further constraints. However, current and currently planned space missions are unfortunately not able to provide such observations. This calls in the need for a specialised space mission to observe stars in their early evolutionary stages.

Our calculations also result in a \(g\)-mode instability region for \(K\)- and \(M\)-type stars, where long period spacings would be expected for \(M\)-type stars in their earliest evolutionary phases. Such pulsations are expected for some time (Rodríguez-López 2019), but to our knowledge, no candidate has been detected from observations yet. We present the case of 2MASS J11112032-7673034, a young stellar object with a spectral type of M5.5. The light curve obtained from the crowded TESS FFIs shows three frequencies attributed to pulsations and additional variability most likely originating from stellar spots. While our grid is sparse in this area of the Kiel diagram we looked for models fitting both, the effective temperature constraints of Gutiérrez Albarrán et al. (2020) and the observed frequencies. We found two models with unstable modes within a fourth of the Rayleigh limit of each of the three frequencies. Because the FFIs are crowded and the obtained light curve is comparatively short, we were not able to simply attribute the observed variability to 2MASS J11112032-7673034 and, hence, we can only suggest that 2MASS J11112032-7673034 may well be the first potential candidate pulsator of this class. TESS will revisit 2MASS J11112032-7673034 in sectors 38 and 39, which should improve our analysis. Once this data becomes available, we strive to obtain an improved picture of the status of this star.

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T. Steindl et al.: Pulsational instability of pre-main-sequence models from accreting protostars. I.

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Appendix A: TESS observations

A.1. Spectral window of TESS and CoRot observation

In the Fourier analysis of time series photometry, the time stamps of observations often introduce alias frequencies due to the convolution of the amplitude spectrum with the spectral window. The spectral window of different light curves analysed in this work is shown in Fig. A.1 - A.3. While there is no signal whatsoever in the spectral window of the TESS observations, there are some small peaks in the CoRot observations. However, their amplitude is small enough that this does not lead to serious aliasing problems in our analysis.

A.2. Frequency tables and FFI images of the newly discovered pre-main-sequence pulsators

In the following, we provide the tables of extracted frequencies for the newly discovered pre-main-sequence pulsators from TESS data (i.e., Tables A.1 to A.5 and the respective full frame images (FFIs) that are described in the main part of the article (i.e., Figures A.4 to A.14).

It is important to state that the reported uncertainties for frequency, amplitude, and phase correspond only to the uncertainties obtained from the modelling of the adopted light curve. Given that different apertures and corrections lead to slightly different light curves, we assume that our uncertainties are strongly underestimated.

A.3. Other variable stars

CD-49 11096 is a B9V (Aidelman et al. 2018) star observed in sector 12. No short-cadence data are available for this star, hence, we use the light curve obtained using the RegressionCorrector. CD-4911096 has a TESS magnitude of 10.584. Multiple other stars lie within the chosen aperture as the sky region is very crowded. Most notably are GAIA DR2 593832402430525696 with a TESS magnitude of 12.277 and GAIA DR2 5938324038039512192 with a TESS magnitude of 11.533 which do not have an entry in the SIMBAD database. We extract two significant frequencies at 5.45237 and 5.53471 d\(^{-1}\) and the amplitude spectrum shows additional signal around 15 and 21d\(^{-1}\) although no frequency is significant in this range. The TIC reports \(T_{\text{eff}} = 6501\) K for one of the two close-by objects, GAIA DR2 5938324038039512192; an effective temperature as would be expected for \(\delta\) Sct stars. Given the frequency ranges, we might see the signal of a pre-main-sequence
Table A.1. Extracted instabilities for the pre-main-sequence SPB star BD+65 1637.

| Designation | f (d⁻¹) | A (mmag) | \(\phi (\pi/2)\) | S/N |
|-------------|---------|----------|------------------|-----|
| F1          | 3.07646(2) | 1.094(12) | 0.854(2)         | 11.53 |
| F2          | 0.507339(4) | 1.085(12) | 0.692(2)         | 13.70 |
| F3          | 2.151676(4) | 1.054(12) | 0.284(2)         | 13.60 |
| F4          | 3.018586(6) | 0.772(12) | 0.555(5)         | 11.60 |
| F5          | 0.199488(12) | 0.374(12) | 0.522(5)         | 5.36  |
| F6          | 2.905707(4) | 0.335(12) | 0.592(6)         | 5.31  |
| F7          | 3.190572(14) | 0.333(12) | 0.731(6)         | 5.74  |
| F8          | 3.261994(14) | 0.334(12) | 0.744(6)         | 6.14  |
| F9          | 5.228138(15) | 0.311(12) | 0.806(6)         | 6.79  |
| F10         | 3.09616(2) | 0.292(12) | 0.500(7)         | 5.40  |
| F11         | 2.98411(2) | 0.273(12) | 0.798(7)         | 5.11  |
| F12         | 5.74287(2) | 0.230(12) | 0.433(8)         | 5.59  |
| F13         | 2.54778(2) | 0.224(12) | 0.425(9)         | 4.34  |
| F14         | 6.09446(2) | 0.210(12) | 0.975(9)         | 5.78  |
| F15         | 6.16729(2) | 0.194(12) | 0.791(10)        | 5.92  |
| F16         | 3.08344(2) | 0.191(12) | 0.846(10)        | 4.00  |
| F17         | 8.59152(3) | 0.161(12) | 0.292(11)        | 8.53  |
| F18         | 10.51292(3) | 0.150(12) | 0.139(13)        | 10.06 |
| F19         | 5.41367(3) | 0.148(12) | 0.870(13)        | 4.12  |
| F20         | 7.32194(3) | 0.134(12) | 0.647(14)        | 6.02  |
| F21         | 5.17067(3) | 0.139(12) | 0.843(14)        | 3.77  |

Notes. The values in parentheses give the 1σ uncertainty as reported by the standard error estimates formulated by Montgomery & O’Donoghue (1999).

Table A.2. Extracted frequencies for the pre-main-sequence SPB candidates found in this work.

| Designation | f (d⁻¹) | A (mmag) | \(\phi (\pi/2)\) | S/N |
|-------------|---------|----------|------------------|-----|
| HD 152822 – candidate |
| F1          | 2.25479(2) | 1.165(5) | 0.153(7)         | 10.56  |
| F2          | 0.84580(4) | 0.735(5) | 0.310(11)        | 6.48   |
| F3          | 2.31573(5) | 0.495(9) | 0.333(17)        | 6.52   |
| F4          | 1.97877(7) | 0.345(5) | 0.403(3)         | 4.93   |
| F5          | 2.47346(3) | 0.315(9) | 0.13(13)         | 5.38   |
| F6          | 4.84655(2) | 0.215(11) | 0.31(4)         | 4.56   |
| F7          | 5.15125(13) | 0.195(5) | 0.09(4)         | 4.68   |
| F8          | 4.51676(14) | 0.185(5) | 0.55(5)         | 4.90   |
| HD 32972 – candidate |
| F1          | 1.405(3) | 1.335(5) | 0.257(6)         | 10.04  |
| F2          | 0.70984(4) | 0.525(5) | 0.433(15)        | 4.75   |
| F3          | 1.16862(7) | 0.355(5) | 0.70(2)         | 4.41   |
| F4          | 2.25479(14) | 0.175(7) | 0.67(5)         | 4.55   |
| F5          | 4.4988(2) | 0.115(5) | 0.68(7)         | 4.64   |
| F6          | 1.49849(2) | 0.255(5) | 0.81(3)         | 3.88   |
| F7          | 1.0898(1) | 0.245(1) | 0.92(3)         | 3.70   |
| F1          | 2.473508(2) | 1.54(6) | 0.301(6)        | 13.84  |
| F2          | 2.51648(8) | 0.365(9) | 0.92(3)        | 5.49   |

Table A.3. Extracted frequencies for the pre-main-sequence \(\gamma\) Doradus candidate HD 317859.

| Designation | f (d⁻¹) | A (mmag) | \(\phi (\pi/2)\) | S/N |
|-------------|---------|----------|------------------|-----|
| HD 329721 – candidate |
| F1          | 2.109(2) | 2.51(13) | 0.912(8)         | 7.44   |
| F2          | 1.37264(4) | 1.48(13) | 0.568(14)        | 6.46   |
| F3          | 2.73471(8) | 0.78(13) | 0.66(3)         | 6.44   |
| F4          | 2.68658(10) | 0.62(13) | 0.43(5)         | 6.28   |
| F5          | 5.4213(2) | 0.28(13) | 0.16(7)         | 4.95   |
| F7          | 5.3775(3) | 0.22(13) | 0.68(10)        | 4.23   |
| F8          | 5.6794(4) | 0.18(13) | 0.47(11)        | 4.33   |
| F9          | 2.4022(2) | 0.28(13) | 0.99(7)         | 3.64   |

Notes. The values in parentheses give the 1σ uncertainty as reported by the standard error estimates formulated by Montgomery & O’Donoghue (1999).

\(\delta\) Scuti star. However, more data will be needed to verify this preliminary identification and we restrain from adding CD-4911096 with \(T_{\text{eff}} = 11450 \pm 308\) K and \(\log(g) = 4.26 \pm 0.12\) to our sample. The FFI and chosen aperture are shown in Fig. A.15.

PDS 344 is most likely a B5 star (Vieira et al. 2003) observed in sector 10 and 11. No short-cadence data are available for this star, hence we use the light curve obtained using the RegressionCorrector. PDS 344 has a TESS magnitude of 13.07. The apertures for sector 10 and sector 11 are slightly shifted with respect to each other, resulting in different stars lying inside the aperture of each sector. Most notably GAIa DR2 5332670397352388608 with a TESS magnitude of 14.374 lies within the aperture in sector 11. We extract one frequency at 6.96842(3) d⁻¹ with an amplitude of 0.69(4) mmag and a S/N of 38.
### Table A.4. Extracted frequencies for the pre-main-sequence δ Scuti stars found in this work.

| Designation | $f$ (d$^{-1}$) | $A$ (mmag) | $\phi$ (rad$^{-1}$) | S/N |
|-------------|---------------|------------|----------------------|-----|
| HD 287823  |               |            |                      |     |
| F1         | 20.32224(5)   | 0.189(17)  | 0.713(14)            | 6.41|
| F2         | 23.74746(5)   | 0.186(17)  | 0.428(14)            | 5.22|
| F3         | 19.69683(7)   | 0.137(17)  | 0.803(19)            | 6.56|
| F4         | 16.41862(8)   | 0.107(17)  | 0.392(2)             | 6.07|
| F5         | 20.998009(9)  | 0.103(17)  | 0.173(5)             | 5.87|
| F6         | 19.06234(11)  | 0.083(17)  | 0.693(5)             | 5.01|
| F7         | 23.22791(12)  | 0.078(17)  | 0.893(3)             | 4.31|
| F8         | 16.14735(13)  | 0.072(17)  | 0.094(4)             | 4.87|
| F9         | 21.40260(13)  | 0.070(17)  | 0.634(4)             | 4.47|
| F10        | 18.65773(14)  | 0.063(17)  | 0.084(4)             | 4.46|
| F11        | 19.44395(18)  | 0.051(17)  | 0.525(5)             | 4.08|
| (F12)      | 23.97275(9)   | 0.100(17)  | 0.73(3)              | 3.58|

### Table A.5. Extracted frequencies for the pre-main-sequence δ Scuti candidates found in this work.

| Designation | $f$ (d$^{-1}$) | $A$ (mmag) | $\phi$ (rad$^{-1}$) | S/N |
|-------------|---------------|------------|----------------------|-----|
| V599 Ori – candidate |               |            |                      |     |
| F1         | 22.72214(3)   | 0.855(17)  | 0.995(9)             | 8.24|
| F2         | 20.92903(7)   | 0.375(5)   | 0.70(2)              | 5.34|
| F3         | 23.46700(8)   | 0.345(5)   | 0.012(5)             | 5.05|
| F4         | 23.75206(8)   | 0.335(5)   | 0.83(2)              | 6.14|
| F5         | 19.38418(4)   | 0.325(5)   | 0.23(2)              | 5.85|
| F6         | 21.76122(9)   | 0.295(5)   | 0.17(3)              | 5.02|
| F7         | 19.22786(10)  | 0.265(5)   | 0.70(3)              | 5.67|
| F8         | 21.03018(11)  | 0.235(5)   | 0.23(5)              | 4.97|
| F9         | 21.68766(13)  | 0.205(5)   | 0.72(4)              | 5.06|
| F10        | 13.14041(13)  | 0.205(5)   | 0.43(4)              | 6.00|
| F11        | 20.22557(13)  | 0.205(5)   | 0.50(4)              | 6.38|
| F12        | 2.84142(15)   | 0.175(5)   | 0.04(5)              | 4.00|
| F13        | 23.21872(17)  | 0.165(5)   | 0.68(5)              | 4.22|
| F14        | 17.61864(18)  | 0.155(5)   | 0.50(5)              | 4.32|
| F15        | 21.3842(2)    | 0.125(5)   | 1.00(6)              | 4.21|
| F16        | 19.87613(3)   | 0.105(5)   | 0.40(8)              | 4.07|
| (F17)      | 1.42999(10)   | 0.25(5)    | 0.49(3)              | 3.85|
| (F18)      | 21.2831(3)    | 0.105(5)   | 0.85(8)              | 3.67|

### HD 144432

| Designation | $f$ (d$^{-1}$) | $A$ (mmag) | $\phi$ (rad$^{-1}$) | S/N |
|-------------|---------------|------------|----------------------|-----|
| F1         | 0.89620(2)    | 2.08(10)   | 0.558(8)             | 8.36|
| F2         | 14.50410(3)   | 1.77(10)   | 0.350(9)             | 14.30|
| F3         | 13.18489(7)   | 0.67(10)   | 0.25(2)              | 11.35|
| F4         | 23.16855(8)   | 0.63(10)   | 0.31(2)              | 11.19|
| F5         | 15.51142(8)   | 0.58(10)   | 0.38(3)              | 9.17|
| F6         | 21.46936(9)   | 0.57(10)   | 0.163(3)             | 12.08|
| F7         | 20.61618(10)  | 0.47(10)   | 0.46(3)              | 11.25|
| F8         | 18.8560(2)    | 0.25(10)   | 0.90(6)              | 6.20|
| F9         | 15.3609(2)    | 0.24(10)   | 0.38(7)              | 6.79|
| F10        | 13.2709(2)    | 0.19(10)   | 0.20(8)              | 6.35|
| F11        | 18.4617(3)    | 0.18(10)   | 0.56(9)              | 5.64|
| F12        | 16.3072(3)    | 0.16(10)   | 0.49(10)             | 4.94|
| F13        | 15.8233(4)    | 0.11(10)   | 0.69(14)             | 4.47|
| (F14)      | 23.3693(4)    | 0.11(10)   | 0.89(14)             | 3.84|
| (F15)      | 18.5406(5)    | 0.09(10)   | 0.31(17)             | 3.54|
| (F16)      | 14.5686(5)    | 0.09(10)   | 0.32(17)             | 3.56|

**Notes.** The values in parentheses give the $1\sigma$ uncertainty as reported by the standard error estimates formulated by Montgomery & O'Donoghue (1999).

We have a clear detection of the frequency, as it is evident in both sectors. However, given the crowded nature of the FFIs we restrained from adding PDS 344 to our sample of pulsating stars. More observations are needed for an identification. The FFI and chosen aperture for sector 10 are shown in Fig. A.16.

**HD 36982** is a B1.5Vp star (according to SIMBAD) observed in sector 6. No short-cadence data are available for this star, hence we use the light curve obtained using the RegressionCorrector. There are no other stars in the aperture, but strong background light from nearby O-type stars can be detected. We extract one frequency at 6.087443(3) d$^{-1}$ with an amplitude of 0.41(3) mmag and a S/N of 11.11. This is similar to...
Fig. A.4. TESS FFI image in a 20×20 pixel cutout around the position of HD 152822 in sector 12. Red filled area shows the chosen aperture. The red dots show stars within a GAIA magnitude limit × 6 with varying size according to their GAIA magnitude. The GAIA query failed for HD 152822 and hence the magnitudes are relative to TYC 8327-955-1, which is marked by the white cross.

Fig. A.5. TESS FFI image in a 20×20 pixel cutout around the position of HD 152799 in sector 12. Red filled area shows the chosen aperture. The red dots show stars within a GAIA magnitude limit × 6 with varying size according to their GAIA magnitude and the white cross marks the position of HD 152799.

Fig. A.6. TESS FFI image and chosen aperture. Same details as in Fig. A.5 but for HD 329271 in sector 12.

Fig. A.7. TESS FFI image and chosen aperture. Same details as in Fig. A.5 but for CD-32 12908 in sector 12.

Fig. A.8. TESS FFI image and chosen aperture. Same details as in Fig. A.5 but for HD 287823 in sector 6.

the case of PDS 344. More observations are needed for an identification. The FFI and chosen aperture for sector 10 are shown in Fig. A.17.

HD 329279 is a B0II star (Aidelman et al. 2018) observed in sector 12. No short-cadence data are available for this star, hence we use the light curve obtained using the RegressionCorrector. There are no other stars in the aperture, however, there are two darker stars in the vicinity from which we expect no contamination. We extract 17 significant frequencies and interpret the light curve and the frequency spectrum as ellipsoidal variability of a close binary system with an orbital period of about 2.25 d. All but five of the extracted fre-
Fig. A.9. TESS FFI image and chosen aperture. Same details as in Fig. A.5 but for HD 290500 in sector 6.

Fig. A.10. TESS FFI image in a $20 \times 20$ pixel cutout around the position of V599 Ori in sector 6. Red filled area shows the chosen aperture and the magenta area shows the chosen pixel for the simple background flux. The red dots show stars within a GAIA magnitude limit $\leq 6$ with varying size according to their GAIA magnitude and the white cross marks the position of V599 Ori. The influence of the naked eye star 49 Ori is clearly visible.

Fig. A.11. TESS FFI image and chosen aperture. Same details as in Fig. A.5 but for TYC 8581-2002-1 in sector 10. Sectors 8 and 9 have also been observed.

Fig. A.12. TESS FFI image and chosen aperture. Same details as in Fig. A.5 but for HD 144432 in sector 6.

Fig. A.13. TESS FFI image and chosen aperture. Same details as in Fig. A.5 but for HD 317859 in sector 12.

Frequencies are multiples of the orbital frequency $F_2$. The others constitute a quartet ($F_3, F_6, F_{13}, F_{16}$) and a singlet $F_{11}$ (see Table A.6). The frequencies $F_3$ and $F_{16}$ and $F_6$ and $F_{13}$, respectively are each split by exactly the orbital frequency while there is a small additional offset of 0.008 $f_{\text{orb}}$ between $F_3$ and $F_6$. Thus, this could also be two doublets that coincide to a quartet. The light curve (see Fig. A.18) clearly shows additional variability that resembles pulsations. We constructed a simple model for the binary light curve using a Savgol filter with a window length of 31. The residuals show an envelope that rises whenever the light curve obtains a maximum. It is difficult to speak on the origin of the observed light curve and frequencies. Multiple explanations are possible that consist of, for instance, tidally trapped pulsations (Handler et al. 2020; Kurtz et al. 2020; Fuller et al. 2020), tidally perturbed
Fig. A.14. TESS FFI image and chosen aperture. Same details as in Fig. A.5 but for 2MASS 11120327-7637034 in sector 12.

Fig. A.15. TESS FFI image and chosen aperture. Same details as in Fig. A.5 but for CD-4911096 in sector 12.

Fig. A.16. TESS FFI image and chosen aperture. Same details as in Fig. A.5 but for PDS 344 in sector 10. The aperture was shifted in sector 11 which leads to having stars 4 and 5 within the aperture.

Fig. A.17. TESS FFI image and chosen aperture. Same details as in Fig. A.5 but for HD 36982 in sector 6. The aperture was shifted in sector 11 which leads to having stars 4 and 5 within the aperture.

Table A.6. Extracted frequencies for HD 329379.

| Designation | $f$ (d$^{-1}$) | $A$ (mmag) | $\phi$ ($\text{deg}$) | S/N |
|-------------|---------------|------------|------------------------|-----|
| F1 = $2f_{orb}$ | 0.889013(15) | 32.3(2) | 0.283(5) | 13.13 |
| F2 = $f_{orb}$ | 0.44451(3) | 14.2(2) | 0.283(11) | 11.25 |
| F3 | 6.30912(14) | 3.5(2) | 0.91(5) | 13.41 |
| F4 = $4f_{orb}$ | 1.7816(2) | 2.2(2) | 0.457 | 5.71 |
| F5 = $6f_{orb}$ | 2.6670(4) | 1.1(2) | 0.351(5) | 5.99 |
| F6 = $F_3 - 2f_{orb}$ | 5.4165(5) | 1.0(2) | 0.721(6) | 7.15 |
| F7 = $8f_{orb}$ | 3.5632(5) | 1.0(2) | 0.621(6) | 6.91 |
| F8 = $14f_{orb}$ | 6.2123(6) | 0.9(2) | 0.791(9) | 8.35 |
| F9 = $10f_{orb}$ | 4.4558(8) | 0.6(2) | 0.83(3) | 6.38 |
| F10 = $13f_{orb}$ | 5.7642(10) | 0.5(2) | 0.73(3) | 6.71 |
| F11 | 7.4885(13) | 0.4(2) | 0.84(3) | 5.58 |
| F12 = $12f_{orb}$ | 5.3305(15) | 0.3(2) | 0.45(5) | 4.92 |
| F13 = $F_3 - 4f_{orb}$ | 4.8275(16) | 0.3(2) | 0.75(3) | 4.29 |
| F14 = $16f_{orb}$ | 7.1013(17) | 0.3(2) | 0.96(3) | 4.77 |
| F15 = $17f_{orb}$ | 7.5459(19) | 0.3(2) | 0.46(4) | 4.82 |
| F16 = $F_3 + 2f_{orb}$ | 7.1982(2) | 0.2(2) | 0.57(3) | 4.72 |
| F17 = $15f_{orb}$ | 6.653(3) | 0.2(2) | 0.79(3) | 4.36 |

Notes. The values in parentheses give the 1$\sigma$ uncertainty as reported by the standard error estimates formulated by Montgomery & O’Donoghue (1999).

pulsations (Reyniers & Smeyers 2003b,a; Steindl et al. 2021), and tidally induced pulsation including heartbeat effects (Fuller 2017). HD 36982 should therefore be studied in more detail. The FFI and chosen aperture for sector 12 are shown in Fig. A.19.

**HD 96042** is a B1Vne star (Houk & Cowley 1975) observed in sectors 10 and 11. No short-cadence data are available for this star, hence we use the light curve obtained using the RegressionCorrector. Two other stars lie within the chosen aperture, but HD 96042 outshines them by four TESS magnitudes. We extracted three significant frequencies in the g-mode ($< 5$ d$^{-1}$) and eight in the p-mode regime ($> 6.5$ d$^{-1}$). Six more frequencies in the g-mode regime are just below our significance criterion. This indicates that multiple g-modes are excited in HD 96042 and a period spacing might be inferred.
with more observational data. Given the stellar parameters of $T_{\text{eff}} = 25000 \pm 1500$ K and $\log(g) = 3.8 \pm 0.2$ (Fairlamb et al. 2015), we classify HD 96042 as a Cepheid star on the main sequence. The FFI and chosen aperture for sector 10 are shown in Fig. A.20 and the frequencies are listed in Table A.7.

**HD 53367** is a B0IV/Ve star (Tjin A Djie et al. 2001) observed in sector 7. Short-cadence data are available, hence, we downloaded the PDCSAP flux from the MAST portal. We extract three frequencies in the g-mode and one additional frequency in the p-mode regime. The residuals show more variability in the low frequency range, hence, further observations of HD 53367 might enable the identification of further modes, similar to HD 96042. Given the stellar parameters of $T_{\text{eff}} = 29000 \pm 2000$ K and $\log(g) = 4$ (Alecian et al. 2013), we classify HD 53367 as a Cepheid star on the main sequence. The frequencies are listed in Table A.8.

**HD 152743** is a B2IV star (Houk 1978) observed in sector 11. No short-cadence data are available for this star, hence we use the light curve obtained using the RegressionCorrector. Five other stars lie within the chosen aperture with up to only one magnitude less than HD 152743. We extract seven significant frequencies clearly indicating g-mode pulsations. With
Table A.8. Extracted frequencies for HD 53367.

| Designation | $f$ (d$^{-1}$) | $A$ (mmag) | $\phi$ (°) | S/N |
|-------------|----------------|------------|-------------|-----|
| F1          | 2.245051(8)    | 0.755(12)  | 0.422(2)    | 7.19|
| F2          | 2.204158(12)   | 0.542(12)  | 0.323(4)    | 6.41|
| F3          | 2.281855(19)   | 0.336(12)  | 0.544(6)    | 5.04|
| F4          | 12.11828(14)   | 0.047(12)  | 0.154(8)    | 4.65|

Notes. The values in parentheses give the 1σ uncertainty as reported by the standard error estimates formulated by Montgomery & O’Donoghue (1999).

Appendix B: Pre-main-sequence $\gamma$ Doradus and hybrid stars discovered from CoRoT data: Frequency tables and spectroscopic data

B.1. Frequency tables

Tables B.1, B.2, and B.3 list the frequencies extracted in the two pre-main-sequence $\gamma$ Doradus stars and the pre-main-sequence $\delta$ Scuti – $\gamma$ Doradus hybrid discovered from CoRoT data.

Table B.1. Extracted frequencies for Cl$^+$ NGC 2264 VAS 196.

| Designation | $f$ (d$^{-1}$) | $A_{SRa05}$ (mmag) | $\phi$ (°) | S/N | cross-ref |
|-------------|----------------|---------------------|-------------|-----|-----------|
| F1          | 0.88674(8)     | 1.344(7)            | 0.465(9)    | 7.83| SRa01, TESS |
| F2          | 1.3664(1)      | 1.029(7)            | 0.434(1)    | 9.75| SRa01, TESS |
| F3          | 1.32171(1)     | 0.762(7)            | 0.353(2)    | 10.99| SRa01, TESS |
| F4          | 1.48189(2)     | 0.519(7)            | 0.621(2)    | 10.99| SRa01 |
| F5          | 0.90832(2)     | 0.451(7)            | 0.062(2)    | 5.84| SRa01 |
| F6          | 0.15694(4)     | 0.289(7)            | 0.750(4)    | 4.06| SRa01 |
| F7          | 1.28741(4)     | 0.548(7)            | 0.657(5)    | 5.07| SRa01 |
| F8          | 2.75115(5)     | 0.212(7)            | 0.660(6)    | 7.14| SRa01 |
| F9          | 1.44205(5)     | 0.233(7)            | 0.558(5)    | 6.22| SRa01 |

Notes. The values in parentheses give the 1σ uncertainty as reported by the standard error estimates formulated by Montgomery & O’Donoghue (1999). The amplitudes ($A_{SRa05}$) are determined from the CoRoT SRa05 data. The last column (cross-ref) marks the frequencies that can also be detected in the CoRoT SRa01 and TESS data.

Table B.2. Extracted frequencies for Cl$^+$ NGC 2264 VAS 219.

| Designation | $f$ (d$^{-1}$) | $A_{SRa05}$ (mmag) | $\phi$ (°) | S/N | cross-ref |
|-------------|----------------|---------------------|-------------|-----|-----------|
| F1          | 2.09926(5)     | 0.407(1)            | 0.227(5)    | 7.37| SRa01, TESS |
| F2          | 1.92554(6)     | 0.341(7)            | 0.091(6)    | 7.05| SRa01, TESS |
| F3          | 1.36574(7)     | 0.277(7)            | 0.342(7)    | 6.44| SRa01, TESS |
| F4          | 0.04759(7)     | 0.251(7)            | 0.840(8)    | 5.93| SRa01 |
| F5          | 0.19931(1)     | 0.188(1)            | 0.120(1)    | 4.57| SRa01 |
| F6          | 0.05621(1)     | 0.196(1)            | 0.103(1)    | 4.72| SRa01, TESS |
| F7          | 1.33921(1)     | 1.388(7)            | 0.290(7)    | 5.02| SRa01 |
| F8          | 2.14811(1)     | 1.888(7)            | 0.521(7)    | 6.10| SRa01 |
| F9          | 3.42814(1)     | 1.62(1)             | 0.416(1)    | 9.91| SRa01 |
| F10         | 1.80491(1)     | 1.58(1)             | 0.302(1)    | 5.32| SRa01, TESS |
| F11         | 3.78101(1)     | 1.50(1)             | 0.301(1)    | 13.95| SRa01 |
| F12         | 0.1067(1)      | 1.571(1)            | 0.929(1)    | 5.00| SRa01 |
| F13         | 1.63591(1)     | 1.45(1)             | 0.303(1)    | 5.01| SRa01 |
| F14         | 0.56011(1)     | 1.49(1)             | 0.277(1)    | 4.19| SRa01 |
| F15         | 2.45391(1)     | 1.34(1)             | 0.327(1)    | 4.88| SRa01 |
| F16         | 1.54512(1)     | 1.24(1)             | 0.416(2)    | 5.10| SRa01 |
| F17         | 0.16621(2)     | 1.00(1)             | 0.329(2)    | 4.26| SRa01 |
| F18         | 1.06082(2)     | 1.11(1)             | 0.554(2)    | 3.74| SRa01 |
| F19         | 0.33891(2)     | 1.03(1)             | 0.218(2)    | 4.10| SRa01 |
| F20         | 2.37822(2)     | 1.01(1)             | 0.961(2)    | 5.07| SRa01 |
| F21         | 0.07732(2)     | 1.77(1)             | 0.278(2)    | 8.98| SRa01 |
| F22         | 1.87152(2)     | 1.00(1)             | 0.119(2)    | 4.93| SRa01 |
| F23         | 1.90702(2)     | 0.89(1)             | 0.316(2)    | 5.51| SRa01 |
| F24         | 1.6848(3)      | 0.72(1)             | 0.751(3)    | 4.26| SRa01 |

Notes. The values in parentheses give the 1σ uncertainty as reported by the standard error estimates formulated by Montgomery & O’Donoghue (1999). The amplitudes ($A_{SRa05}$) are determined from the CoRoT SRa05 data. The last column (cross-ref) marks the frequencies that can also be detected in the CoRoT SRa01 and TESS data.

$T_{\text{eff}} = 24600 \pm 2371 \text{ K}$ and $\log(g) = 3.76 \pm 0.34$ (Aidelman et al. 2018), HD 152743 could very well be the source of these g-mode pulsations. However, some of the other stars also have effective temperatures expected for g-mode pulsators according to the TIC. Hence, additional observations are needed for a clear identification. The FFI and chosen aperture for sector 10 are shown in Fig. A.21 and the frequencies are listed in Table A.9.

Fig. A.21. TESS FFI image and chosen aperture. Same details as in Fig. A.5 but for HD 152743 in sector 12.
Table B.3. Extracted frequencies for CI* NGC 2264 VAS 230.

| Designation | $f$ (d$^{-1}$) | $A_{SRa01}$ (mmag) | $\phi$ (mm) | S/N | cross ref |
|-------------|---------------|--------------------|-------------|-----|-----------|
| F1          | 8.1866(4)     | 0.77(1)            | 0.336(3)    | 6.71 | SRa05, TESS |
| F2          | 8.4660(6)     | 0.62(1)            | 0.730(3)    | 9.10 | SRa05, TESS |
| F3          | 8.5591(8)     | 0.42(1)            | 0.891(4)    | 7.98 | SRa05, TESS |
| F4          | 11.8419(9)    | 0.35(1)            | 0.175(6)    | 10.87| SRa05, TESS |
| F5          | 8.3851(1)     | 0.29(1)            | 0.46(4)     | 6.33 | TESS      |
| F6          | 2.3203(7)     | 0.58(1)            | 0.28(2)     | 4.18 | SRa05     |
| F7          | 2.2407(6)     | 0.54(1)            | 0.65(4)     | 5.07 | SRa05     |
| F8          | 2.1643(6)     | 0.49(1)            | 0.71(3)     | 4.15 | SRa05     |
| F9          | 3.3006(8)     | 0.46(1)            | 0.27(5)     | 5.48 | SRa05     |

Notes. The values in parentheses give the 1σ uncertainty as reported by the standard error estimates formulated by Montgomery & O’Donoghue (1999). The amplitudes ($A_{SRa01}$) are determined from the CoRoT SRa01 data. The last column (cross ref) marks the frequencies that can also be detected in the CoRoT SRa05 and TESS data. The first five frequencies are the p-modes and the second four frequencies are the g-modes; both are sorted by decreasing amplitude.

Table B.4. Fundamental parameters for the six pre-main-sequence γ Doradus stars discovered from CoRoT data.

| Identifier          | $T_{\text{eff}}$ (K) | log(g) (dex) | $v\sin i$ (km s$^{-1}$) | [Fe/H] (dex) |
|---------------------|----------------------|--------------|-------------------------|--------------|
| CI* NGC 2264 VAS 196 | 6784(150)            | 4.0(2)       | 77(5)                   | -0.072       |
| CI* NGC 2264 VAS 219 | 7170(150)            | 4.3(3)       | 74(5)                   | -0.286       |
| CI* NGC 2264 VAS 230 | 7520(150)            | 4.3(4)       | 205(25)                 | -0.200       |

B.2. High-resolution spectroscopy: observations, data reduction, and analysis

We obtained high-resolution spectra with the Robert G. Tull Coudé spectrograph (TS) on the 2.7-m telescope of Mc Donald Observatory for CI* NGC 2264 VAS 196 (CoID0223991870) and CI* NGC 2264 VAS 219 (CoID0223997565). The cross-dispersed échelle spectrograph has a resolving power of 60000 in the configuration adopted by us. Each spectrum covers the wavelength range from 3633 to 10 849 Å with gaps between the échelle orders at wavelengths longer than 5870 Å. The spectra for the two stars have signal-to-noise (S/N) ratios of 84 and 80, respectively, calculated at ~5240 Å.

Bias and Flat Field frames were obtained at the beginning of each night, while several Th-Ar comparison lamp spectra were obtained each night for wavelength calibration purposes. The reduction was performed using the Image Reduction and Analysis Facility (IRAF). The spectra were normalized by fitting a low order polynomial to carefully selected continuum points.

For CI* NGC 2264 VAS 230 (CoID0223999101) and CI* NGC 2264 VAS 196 (CoID 0223991870), a spectrum obtained with the cross-dispersed échelle spectrograph UVES at the ESO Very Large Telescope (VLT) was available in the ESO archive. UVES has a resolving power of 40000 in the standard mode. All reduction steps were performed within the UVES pipeline (version 5.2.0) and the Reflex software. The UVES spectra for CI* NGC 2264 VAS 230 (CoID0223999101) and CI* NGC 2264 VAS 196 have S/N values of 139 and 157 calculated at ~5845 Å, respectively.

The spectroscopic analysis was performed using the LLLMODELS model atmosphere code (Shulyak et al. 2004), the VALD database for atomic line parameters (Kupka et al. 1999), SYNTH3 (Kuchikhov et al. 2007) for the computation of synthetic spectra and an updated version of the Spectroscopy Made Easy (SME, version 474) software package (Valenti & Piskunov 1996; Piskunov & Valenti 2017). Using these methods for each of the three pre-main-sequence pulsators, the effective temperature, surface gravity, projected rotational velocity, and metallicity were determined. A detailed description of the adopted procedure can be found, for example, in Zwińcz et al. (2017b).

CI* NGC 2264 VAS 196 (CoID 0223991870): For this star, two spectra are available: one obtained at Mc Donald Observatory and one observed with the UVES spectrograph at the VLT that we retrieved from the ESO archive. As the S/N value of the UVES spectrum (i.e., 157) is significantly higher than that of the spectrum from Mc Donald observatory (i.e., 50), we base our analysis on the UVES spectrum. We determine a $T_{\text{eff}}$ of 6784 ± 150 K and a log(g) of 4.0 ± 0.2. The star rotates moderately fast with a $v\sin i$ of 77 km s$^{-1}$ and it shows basically solar chemical abundances. The observed and synthetic spectra are shown in Fig. B.1.

CI* NGC 2264 VAS 230 (CoID 0223997565): The spectrum obtained at Mc Donald observatory for CI* NGC 2264 VAS 219 shows many emission lines (as can be seen in Fig. B.2). Our analysis yielded a $T_{\text{eff}}$ of 7170 ± 150 K, a log(g) of 4.3 ± 0.3, a $v\sin i$ of 74 ± 5 km s$^{-1}$, and slightly less than solar abundance. The observed and synthetic spectra are shown in Fig. B.2.

CI* NGC 2264 VAS 230 (CoID 0223999101): The UVES spectrum retrieved from the ESO archive shows that CI* NGC 2264 VAS 230 has an extremely high $v\sin i$ value. This makes it challenging to determine reliable values for the star’s fundamental parameters. Our best-fitting spectrum synthesis model yields a $T_{\text{eff}}$ of 7520 ± 150 K, a log(g) of 4.3 ± 0.4, and a $v\sin i$ of 205 ± 25 km s$^{-1}$ with slightly less than solar abundance. The observed and synthetic spectra are shown in Fig. B.3.

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5 IRAF (http://iraf.noao.edu) is distributed by the National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy (AURA) under cooperative agreement with the National Science Foundation.

6 http://archive.eso.org

7 http://www.eso.org/sci/software/reflex

8 http://valid.astro.uu.se
Radiative opacities are primarily from OPAL (Iglesias & Rogers 1993, 1996), with low-temperature data from Ferguson et al. (2005) and the high-temperature, Compton-scattering dominated regime by Buchler & Yueh (1976). Electron conduction opacities are from Cassisi et al. (2007).

Nuclear reaction rates are a combination of rates from NACRE (Angulo et al. 1999), JINA REACLIB (Cyburt et al. 2010), plus additional tabulated weak reaction rates Fuller et al. (1985), Oda et al. (1994), Langanke & Martinez-Pinedo (2000). Screening is included via the prescription of Chugunov et al. (2007). Thermal neutrino loss rates are from Itoh et al. (1996).

Appendix D: Instability regions

In the following, we show instability results resulting from our calculations. Figures D.1 and D.2 show the influence of the mixing length on the instability regions of p-modes and g-modes, respectively. Figure D.3 shows the comparison between classical models and the models from accreting protostars.

**Appendix C: MESA microphysics**

The MESA EOS is a blend of the OPAL Rogers & Nayfonov (2002), SCVH Saumon et al. (1995), PTEH Pols et al. (1995), HELM Timmes & Swesty (2000), and PC Potekhin & Chabrier (2010) EOSes.
Fig. D.3. Comparison of the instability regions from accreting models versus classical models. The dashed line is the evolutionary track from the accreting model. Black lines show the evolutionary tracks of classical models and the colour code is the same as in Fig. 11. The red lines show the border of instability regions of the classical model while the blue lines show the same borders as in Fig. 11.