Numerical Simulation of Jet Pipe Servo Valve

Ying ZHANG, Junshuo CHEN

Abstract: The jet pipe servo valve (jet valve) is the most widely used flow control servo valve on aircrafts and space crafts. However, the valve has not been simulated accurately due to its special structure and complex internal flow field. The structure design and performance analysis of the valve mainly rely on repeated experiments, which greatly limits the development efficiency of the valve. To solve the problem, this paper analyzes the magnetic field, flow field and structure field, all of which are involved in the working of the valve, one by one, and numerically simulate the coupling of the three fields. The simulated results were verified through experiments. Our method can greatly enhance the accuracy of jet valve simulation, providing a good reference to the simulation of various complex electrohydraulic devices.

Keywords: coupling; flow field; jet pipe servo valve (jet valve); magnetic field; numerical simulation; structure field

1 INTRODUCTION

Flow control servo valve, a key component on aircrafts and space crafts, has been widely used in many fields [1]. Jet pipe servo valve (jet valve) and nozzle flapper valve are the most commonly used two-stage flow control servo valves. The jet valve outperforms the nozzle flapper valve in many aspects, including the self-centering function under failure, the excellence in pollution resistance, the high sensitivity and resolution, and the ability to operate at low voltage [2-4]. As a result, the jet valve has been extensively applied in national defence industry.

The research on jet valves started late in China. The relevant studies are not systematic and are rarely published abroad. The research focus is largely directed to failure reduction by improving processing technique and changing materials [5-8]. China also lags far behind developed countries in the manufacturing of jet valves. The domestic production of jet valves is basically the imitation of imported products. No. 704 Research Institute, China Shipbuilding Industry Corporation (CSIC) is the only company in China capable of producing jet valves.

The inadequate research and backward technique are partly attributable to the complex structure of the jet valve, which is often dubbed as complex electromechanical equipment. To make matters worse, the working process of the valve involves multiple fields, ranging from structure field, electromagnetic field to flow field. The workspace of the valve is always subjected to combined effects of various factors [9-11], making it difficult to determine and predict the valve performance.

At present, there is no report in China about effective mathematical model of the jet valve. Hence, jet valve research mainly relies on repeated experiments, which consume a huge amount of manpower and materials [12]. This calls for a precise and effective way to simulate the jet valve [13] that can be extended to improve the performance of complex electrohydraulic devices with similar structures.

The traditional modelling process generally simplifies the device structure and ignores the complex influencing factors. This is obviously not suitable for such a complex device as jet valve, which often works under harsh conditions. It is impossible to model the jet valve only by theoretical derivation and experiment. The high-precision numerical simulation offers a desirable way to make the impossible possible [14, 15]. For example, the finite-element method and finite-volume method, two typical numerical simulation strategies, can describe every detail of the device, and achieve a precision unmatched by traditional methods.

Some scholars have carried out relevant researches. Li Ruping used CFD (Computational Fluid Dynamics) to analyse the flow field characteristics of jet pipe servo valve in different working media. Xie Zhigang used CFD to simulate the flow field of jet amplifier in jet pipe servo valve in different states [16-18]. However, the current simulation of the jet pipe servo valve is still static; how to describe the dynamic working process of the jet pipe servo valve with numerical method is still a difficulty.

In light of the above, this paper analyses the magnetic field, flow field and structure field, all of which are involved in the working of the valve, one by one, and numerically simulates the coupling of the three fields. The simulated results were verified through experiments. Our method can greatly enhance the accuracy of jet valve simulation, providing a good reference to the simulation of various complex electrohydraulic devices.

2 SYSTEM STRUCTURE AND WORKING PRINCIPLE

Fig. 1 illustrates the structure of the jet valve studied in this research.

As shown in Fig. 1, the jet valve mainly consists of a permanent magnetic moving-iron torque motor, a jet amplifier, a spool assembly and a feedback component. The four components work coordinatively through force feedbacks.

Once the jet tube is deflected, the nozzle at the end of the tube will spray high-pressure oil into two bundles through the two holes beneath the nozzle. The oil in the two bundles will respectively enter the left and right chambers of the spool through the corresponding oil passages [19].

The deflection of the jet tube will make the nozzle deviate from the neutral position of the receiver, causing a difference in the flow rate into the two receiving holes. Thus, there will be a pressure difference between the left and right chambers of the spool. Under the pressure difference, the spool will move and open the oil passage connected to the load chamber.
Due to the movement of the spool, the feedback component will deform which hinders the armature deflection and achieves equilibrium. At this time, the opening size of the valve remains constant. In this way, the load flow can be controlled through current adjustment [20, 21].

3 INDEPENDENT FIELD MODELING AND SIMULATION

This section analyses the fields involved in the working of the jet valve separately, including the magnetic field distribution after the torque motor is energized, the jet flow field distribution of the jet amplifier, the turbulent flow field distribution between the valve sleeves, and the displacement field distribution of the armature feedback rod assembly when the force is deformed.

3.1 Modelling and Numerical Analysis of Magnetic Field

The torque motor has a special spatial structure. Any change to the design or dimension of the structure will greatly affect the distribution of the internal magnetic field. In addition, the boundary conditions of the magnetic field will change in real time with the deflection of the armature. These influencing factors can be fully considered through numerical analysis with 3D model.

Therefore, Maxwell 3D transient analysis was performed to simulate the internal magnetic field of the torque motor under the rotation of the armature. Considering the electromagnetic eddy current and magnetic flux leakage, the torque motor was meshed into grids with high precision at the air gap. To ensure the meshing accuracy, the grids were corrected against the discontinuity degree of the approximate solution on the interface of the adjacent element. The distribution of magnetic field was solved by transforming the large differential equations between grid nodes into algebraic equations through finite-element method. Furthermore, the relationship between the output torque and the off-angle of the armature was obtained by calculation of the independent field, creating a coupling relationship with the structural dynamics. The 3D model of the torque motor and the meshed grids of the magnetic field are shown in Fig. 2 below, where different materials are in different colours.

The material of the four permanent magnets (blue) is Alnico52, its remanence can reach 1.3 T, and its coercive force is 52 kA/m. The upper and lower magnets and armature (pink) are made of soft magnetic alloy 1J50 which is easy to magnetize. The number of turns of the copper coils (orange red) wound on the armature is 730, the relative permeability is 1, and the conductivity is $58 \times 10^6$ Sm$^{-1}$.

By the finite-element method, the transient magnetic field was fully meshed into a myriad of tiny grids. The partial differential equations and boundary conditions of all grid nodes were established. Then, the differential equations were transformed into a linear equation system that can be processed on computer to obtain the magnetic field value of each node in field. The transient computation of 3D magnetic field covers not only transient electromagnetic processes, but also transient mechanical processes, because the transient mechanical deformation directly bears on the transient boundary of the magnetic field. During the computation, the armature angle was limited in the range of $(-1.4^\circ; 1.4^\circ)$, considering the small
size of the air gap. To process mechanical transients, the displacement or angle should be expressed in discrete form:

$$\frac{dx}{dt} = \frac{x^{t+\Delta t} - x^t}{\Delta t}$$  (1)

where, $x$ is the angular displacement of the armature. This nonlinear problem can be solved by the Newton-Raphson iteration method.

Under the step current of 40 mA, the armature will deflect counter clockwise. Fig. 3 shows the field distribution of the armature with the deflection of 0.5°.

The magnetic field is coupled with the structural deformation as follows: First, the magnetic field generates the electromagnetic moment, which acts on the armature; next, the armature deflects in the air gap, changing the boundary of the magnetic field; finally, the magnetic field is redistributed. Mathematically, the core of the coupling mechanism can be described as the relationship between the output torque of the magnetic field and the deflection of the armature angle.

The step currents of 10 mA, 20 mA, 30 mA and 40 mA are respectively applied to the coil, and the output electromagnetic torque change with the deflection of the armature is shown in Tab. 1.

| Torque / Nm | Input current / A |
|------------|-------------------|
| 0          | 0.0019            |
| 0.1        | 0.00411           |
| 0.2        | 0.00627           |
| 0.3        | 0.00834           |
| 0.4        | 0.1040            |
| 0.5        | 0.1259            |

| Nozzle angle / ° | Torque change with the nozzle angle |
|------------------|------------------------------------|
| 0                | 0.0198                           |
| 0.1              | 0.0381                           |
| 0.2              | 0.0575                           |
| 0.3              | 0.0988                           |
| 0.4              | 0.1198                           |
| 0.5              | 0.1459                           |

So the relationship between the torque, current and deflection angle can be expressed as follows:

$$M_d = 1.92i_c + 12.03\theta$$  (2)

where, $M_d$ is the torque applied to the armature by the magnetic field; $i_c$ is the control current; $\theta$ is the armature angle.
separated air (air xichu). Among them, the oil is the primary phase, while the other two phases are secondary. The air density and dynamic viscosity were set to 1,225 kg/m³ and 1,789,4 e-5 kg/ms. The quality transfer can be written as a user-defined function (UDF) below:

\[
\begin{align*}
\text{if}(C_{\text{VOF}}(\text{cell,air_rong})>(C_{\text{P}}(\text{cell,mix})/kx)) \{
\text{m}_l &= 1/\text{step}*(C_{\text{VOF}}(\text{cell,air_rong})-C_{\text{P}}(\text{cell,mix})/kx)*C_{\text{R}}(\text{cell,air_rong}); \\
\text{return m}_l;
\}
\end{align*}
\]

Fig. 4 shows the volume fraction of the gas in the jet flow field when the initial air dissolution volume is 10% and the nozzle is in the neutral position.

Under the deflection of the jet amplifier, the boundary of the jet flow field will change, which in turn alters the pressure difference between the two bundles on both sides, causing displacement of the spool. The spool displacement will further change the flow field boundary of valve sleeves. The coupling mechanism can be described by the relationship between the following factors: the pressure difference of the two bundles, the spool displacement and the deflection of the nozzle. Among them, the spool displacement can be obtained from the load flow of the jet amplifier. Thus, the flow and pressure features of the jet amplifier should be characterized at various times in the deflection process. The cloud maps of pressure in the flow field are given in Fig. 5, when the armature is at the neutral position.

According to the calculation, with the nozzle deflection the pressure difference between the two receiving holes is shown in Tab. 2.

| Table 2 Pressure difference with nozzle angle |
|----------------------------------------------|
| Nozzle angle / ° | 0  | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 |
| Pressure difference / Pa | 5885 | 6964656 | 11106158 | 13026280 | 13713459 | 15373052 |

The flow characteristics of jet amplifier at no load can be calculated by connecting two receiving holes. The cloud chart of flow velocity at no load is shown in Fig. 6.

According to Tab. 2 and Tab. 3, the following function can be derived:

\[
\begin{align*}
p_f &= 6.55\times10^{11}x_j - 2.835\times10^{12}Q_l - 3.59\times10^9\theta - 2.835\times10^{12}\times\dot{x}_v\times A_v \\
&= 1.65\times10^{11}x_j - 2.835\times10^{12}Q_l - 3.59\times10^9\theta - 2.835\times10^{12}\times\dot{x}_v\times A_v
\end{align*}
\]

where, \(p_f\) is the pressure difference of the two bundles; \(x_j\) is the armature offset; \(Q_l\) is the load flow rate; \(\theta\) is the offset angle of the armature; \(\dot{x}_v\) is the spool velocity; \(A_v\) is the effective cross-sectional area of the spool.

(2) Numerical analysis on the flow field of spool sleeves

Once the jet valve is unloaded, the spool will move between the sleeves and the load window, and then the high-pressure oil between the sleeves will flow into the load chamber. When the force reaches the equilibrium, the flow output will become constant after the spool stops. The oil rushing will produce steady-state hydraulic power, the main source of system damping on the spool. Therefore, the analysis on the flow field of spool sleeves is equivalent

![Figure 5](image1)

![Figure 6](image2)

![Figure 4](image3)
to setting up the relationship between opening displacement, load flow and steady-state hydraulic power. Fig. 7 presents the flow distribution when the valve moves slowly to the right at 2 μm/s and gradually opens to 1 mm, and a flow passes between the two load ports.

The flow curve was plotted through data processing for the valve opening of less than 2 μm.

Fig. 7 Flow distribution cloud map

Fig. 8 shows a significant nonlinear relationship between spool displacement and load flow at the initial phase of spool opening, which contradicts the linear relationship in the empirical formula. Since the steady-state hydraulic power of the oil at the opening acts on the valve shoulder, the exact value of the power can be obtained from the mean force on the shoulder. Thus, the relationship between load flow and spool displacement was set up, offering an accurate source of damping for the dynamics analysis of the spool.

The material is given as follows: the material of the nozzle, spring tube, feedback rod and disc is beryllium bronze, its Young's modulus is 1.3×10^5 MPa, Poisson's ratio is 0.35, density is 8230 kg/m^3, yield strength is 1.128×10^3 MPa; The material of the armature is 1J50, its Young's modulus is 1.57×10^5 MPa, the density is 8200 kg/m^3; The supporting reed material is 3J1, the density is 8000 kg/m^3, the Young's modulus is 1.9×10^5 MPa, and the yield strength is 1.9×10^3 MPa; The jet tube material is 1Cr18Ni9Ti, the density is 7900 kg/m^3, the Young's modulus is 1.8×10^5 MPa, and the yield strength is 5.4×10^2 MPa.

By this analysis method, the deformation law of the moving member of the valve was obtained indirectly under the coupling of the electromagnetic force and the fluid force. Meanwhile, the unidirectional coupling between the magnetic field of the armature and the flow field of the valve was described accurately. Since the displacement will be counteracted to the other physical quantities, the armature displacement and spool displacement were taken as the core calculation parameters. The relationships between the displacements and external forces can be expressed as:

\[
\begin{align*}
    x_v &= -1.1 \times 10^{-3} M_f + 3.981 \times 10^{-4} F \\
    x_f &= 9.7228 \times 10^{-4} M_f - 2.398 \times 10^{-5} F
\end{align*}
\]

where, \( M_f \) is the electromagnetic force; \( F \) is the fluid force on the spool.

3.3 Calculation of Structure Field

The working principle of the jet valve is to balance the structural forces, and achieve the one-to-one correspondence between the control current and the opening of the load chamber. During the operation, the valve structure withstands both fluid force and the electromagnetic force, which respectively acts on the armature and the valve. Since the deformation stabilization depends on the feedbacks from relevant components, the stabilization effect directly relies on the accuracy of the feedback information.

The components involved in the feedback include: zero adjustment wire, tubing, reed, feedback rod assembly, etc. The complex structure and unique spatial positions of these components need to be analysed with the 3D model. In this paper, the 3D numerical calculation is applied to determine the stiffness matrix of the grid structure, and differential equations are written by the virtual work principle for finite-element calculation. During the calculation, it is assumed that the armature surface was applied with a 0.15 N electromagnetic force, while the two ends of the valve were each applied with a 0.5 N fluid force Fig. 9. Besides, the lower ends of the leaf springs, the zero adjustment wire, the tubing and the spring tube are fixed.

Fig. 9 Displacement at the electromagnetic force of 0.15 N-m and the fluid force of 0.5 N.

The components involved in the feedback include: zero adjustment wire, tubing, reed, feedback rod assembly, etc. The complex structure and unique spatial positions of
3.4 Numerical Calculation Based on ANSYS Parametric Design Language (APDL) Programming

The working of the jet valve is essentially the coupling between the magnetic field, the flow field and the structure field. Specifically, the torque motor generates magnetic field force to drive the armature deflection, the armature deflection changes the jet flow field boundary of the jet amplifier, and then the pressure difference between the two chambers of the spool causes the spool to move. The spool movement will, on the one hand, block the armature through the feedback rod, and, on the other hand, open the passage between the oil source and the load chamber. As a result, the oil will flow into the load chamber, which produces the hydraulic power to curb the spool displacement.

The constraints applied in the numerical calculation are displayed in Fig. 10. Specifically, A represents the force on the armature; B defines the surface to apply the pressure difference and obtain the spool velocity; C, D and E respectively fix the reeds across the armature, the zero wire, the tubing, and the lower end of the spring tube; F defines the surface to acquire the deflection angle of the nozzle.

The visual simulation was carried out according to the program in the APDL file, which contains the grid meshing, material properties, constraints, boundary conditions and solution methods. In light of the previous analysis, the armature is under the output torque of the torque motor, which is related to the deflection angle of the armature and the input current Eq. (2). According to Eq. (4), the pressure difference across valve is already known. Moreover, the jet nozzle deflection angle is related to the spool velocity. For the armature-feedback rod assembly, the transient dynamics method was selected due to the constant changes to the load on the armature and the spool. Fig. 10 presents the spool and nozzle displacements simulated at the input current of 15 mA.
Ying ZHANG, Junshuo CHEN: Numerical Simulation of Jet Pipe Servo Valve

armature and the input current Eq. (2). According to Eq. (4), the pressure difference across valve is already known. Moreover, the jet nozzle deflection angle is related to the spool velocity. For the armature-feedback rod assembly, the transient dynamics method was selected due to the constant changes to the load on the armature and the spool. Fig. 10 presents the spool and nozzle displacements simulated at the input current of 15 mA.

It can be seen from Fig. 11 that the system was basically stable at 0.02 s, the nozzle displacement peaked at 0.0024 s and then dropped back close to the zero position, and the spool became stable at 0.466 mm.

4 EXPERIMENTAL VERIFICATION

4.1 Design of Remote Wireless Debugging Software

As shown in Fig. 12, a valve flow test platform was set up to test the oil flow between the sleeves. The test platform mainly contains a hydraulic console, a hydraulic oil source system, a hydraulic oil source system, a spool installation and drive system and a computer measurement and control system. Among them, the hydraulic console offers various indicator lights, buttons and display instruments, plus a sliding valve drive system; the hydraulic oil source system provides the test platform with pressure and oil; the oil temperature control system keeps the oil temperature constant through the measurement; the spool installation and drive system mainly fixes the spool with a clamp and drives its movement with a high-precision stepping motor and a ball screw pair, providing an important guarantee of measuring accuracy; the computer measurement and control system collects signals through the test via the conditioning circuit, and processes and displays the acquired signals.

![Figure 13 Picture of laboratory bench](image)

During the test, Y-H 15 aviation hydraulic oil was supplied at 21 MPa ± 0.05 MPa and controlled within 25 °C ± 3 °C. The pollutant level of the oil satisfies the requirement in the national standard GJB420A-1996.

The photo of test platform is shown in Fig. 13.

As shown in Fig. 14, the test results and the calculation results of the flow rate when the spool moves from the initial position to the right by 131 μm are compared. Obviously, the test results were basically the same with the simulated results. When the valve opening is 0 - 100 μm, the error meets the requirements. The existence of small errors is inevitable because the test valve cannot act as an ideal zero-opening valve.

5 CONCLUSIONS

The working process of jet pipe servo valve is very complex, involving the interaction of three physical fields. The traditional lumped parameter model cannot accurately predict the performance of servo valve, which hinders the localization of jet pipe servo valve. In order to improve the prediction accuracy of the performance of jet pipe servo valve, based on the basic theory of magnetic field, flow field and structural field, this paper adopts the numerical calculation method based on unstructured grid to simulate the working process of servo valve dynamically. The numerical results are compared with the traditional lumped parameter method. Through some experimental verification methods, the numerical calculation method adopted in this paper is verified to have high accuracy.

The method used in this paper can be applied to the performance prediction of similar composite electro-hydraulic equipment.

Acknowledgements

Supported by the National Natural Science Foundation of China (Grant No. 51805403).

6 REFERENCES

[1] Zhao, J., Zhang, B., & Chen, T. (2019). Research on valve core’s clamping stagnation of double flapper-nozzle servo valve. High Technology Letters, 25(1), 65-73. https://doi.org/10.3772/j.issn.1006-6748.2019.01.009
[2] Zuo, X., Ruan, J., & Sun, J. (2017). Stability Analysis of 2D Electro-hydraulic Pressure Servo Valve Based on Squeeze Oil Film Theory. Zhongguo Jixie Gongcheng / China Mechanical Engineering, 28(5), 537-543. https://doi.org/10.3969/j.issn.1004-132X.2017.05.006
[3] He, C., Liu, Y., & Yavuzkurt, S. (2018). Large-Eddy Simulation of Circular Jet Mixing: Lip- and Inner-ribbed Nozzles. Computers & Fluids, 168, 245-264. https://doi.org/10.1016/j.compfluid.2018.04.018
[4] Wu, L., Chen, K., & Guo, Y. (2019). Research on cavitation phenomena in pilot stage of jet pipe servo-valve with a rectangular nozzle based on large-eddy simulations. AIP Advances, 9(2), 025109. https://doi.org/10.1063/1.5038402
[5] Wang, Y. & Yin, Y. (2019). Performance reliability of jet pipe servo valve under random vibration environment. Mechatronics, 64, 102286. https://doi.org/10.1016/j.mechatronics.2019.102286
[6] Wu, L., Chen, K., & Zhan, C. (2018). Snapshot POD analysis of transient flow in the pilot stage of a jet pipe servo valve. *Journal of Turbulence*, 19(10), 889-909. https://doi.org/10.1080/14685248.2018.1524579

[7] Zhang, K., Yao, J. Y., & Jiang, T. M. (2014). Degradation assessment and life prediction of electro-hydraulic servo valve under erosion wear. *Engineering Failure Analysis*, 36, 284-300. https://doi.org/10.1016/j.engfailanal.2013.10.017

[8] Hu, J., Yang, Z., Huang, Z., Jin, Y., Yu, B., & Kong, X. (2018). Flow measurement for the pre-stage of jet pipe servo valve using 2D-PIV technique. *International Journal of Fluid Power*, 19(3), 165-172. https://doi.org/10.1080/14399776.2018.1514931

[9] Filo, G., Lisowski, E., & Rajda, J. (2019). Flow analysis of a switching valve with innovative poppet head geometry by means of CFD method. *Flow Measurement and Instrumentation*, 79, 101643. https://doi.org/10.1016/j.flowmeasinst.2019.101643

[10] Li, Y. (2016). Mathematical modelling and characteristics of the pilot valve applied to a jet-pipe/deflector-jet servovalve. *Sensors & Actuators A Physical*, 245, 150-159. https://doi.org/10.1016/j.sna.2016.04.048

[11] Wu, L., Chen, K., & Zhan, C. (2018). Snapshot POD analysis of transient flow in the pilot stage of a jet pipe servo valve. *Journal of Turbulence*, 19(10), 889-909. https://doi.org/10.1080/14685248.2018.1524579

[12] Kang, S., Yan, H., Li, C., Wang, F., & Wang, S. (2017). Modeling of the flow distribution and characteristics analysis of the pilot stage in a deflector jet servovalve. *Journal of Harbin Engineering University*, 38(8), 1293-1302. https://doi.org/10.11990/jheu.201605009

[13] Chen, J., Yuan, Z., Guo, Q., Chu, Y. (2017). Dynamic flow field analysis of the prestage of jet pipe servo valve. *Chinese Journal of Scientific Instrument*, 38(7), 1731-1737.

[14] Ding, Y., Jin, Y., Zhang, X., Wei, T., & Xie, Z. (2016). The design of the integrated jet-pipe servo-valve with high reliability. *IEEE International Conference on Aircraft Utility Systems*, 16484921. https://doi.org/10.1109/AUS.2016.7748197

[15] Zhang, Q., Yan, L., & Duan, Z. (2020). High Torque Density Torque Motor with Hybrid Magnetization Pole Arrays for Jet Pipe Servo Valve. *IEEE Transactions on Industrial Electronics*, 67(3), 2133-2142. https://doi.org/10.1109/TIE.2019.2903761.

[16] Xu, M., Zeng, S., & Guo, J. (2014). Reliability modeling of a jet pipe electrohydraulic servo valve. 2014 *Reliability and Maintainability Symposium*, 1-6. https://doi.org/10.1109/RAMS.2014.6798480

[17] Pham, X. H. S., Yin, Y., & Zhang, X. (2012). Optimal Design for Torque Motor of Jet Pipe Electro-hydraulic Servo-valve Based on Dynamic Stiffness. *International Conference on Intelligent Human-machine Systems & Cybernetics*, 2, 183-186. https://doi.org/10.1109/IHMSC.2012.140

[18] Carla, B. & Giuseppe, P. (2017). Numerical multiphysics modelling for the assessment of thermo-physical and energy performance of an advanced semi-opaque active façade, *International Journal of Heat and Technology*, 33(1), 639-644. https://doi.org/10.18280/ijht.350522

[19] Tian, F., Cao, W. D., Dai, X. L., & Ou, M. X. (2018). Flow characteristics of the new type of mixer in wastewater treatment. *International Journal of Heat and Technology*, 36(3), 913-918. https://doi.org/10.18280/ijht.360318

[20] Garg, R., Thakur, H., & Tripathi, B. (2018). Numerical simulation of two-dimensional fluid flow problem using truly mesh free method. *Mathematical Modelling of Engineering Problems*, 5(4), 357-364. https://doi.org/10.18280/mmeep.050412

[21] Gomboc, T. & Zadravec, M. (2018). Numerical model of three stage spray drying for zeolite 4A-water suspensions coupled with a CFD flow field. *International Journal of Simulation Modelling*, 17(3), 217-228. https://doi.org/10.2507/IJSIMM18(2)462

Contact information:

Ying Zhang, Doctor, (Corresponding author)
School of Optoeletronic Engineering, Xi'an Technological University, Xi'an 710021, China
E-mail: zhangying_1102@163.com

Junshuo Chen, Doctor,
School of Electronic Control, Chang'an University,
Xi'an, 710064, China
E-mail: jsch@chd.edu.cn