Gender Classification from ECG Signal Analysis using Least Square Support Vector Machine

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Abstract  In this present paper it deals with the Gender Classification from ECG signal using Least Square Support Vector Machine (LS-SVM) and Support Vector Machine (SVM) Techniques. The different features extracted from ECG signal using Heart Rate Variability (HRV) analysis are the input to the LS-SVM and SVM classifier and at the output the classifier, classifies whether the patient corresponding to required ECG is male or female. The least square formulation of support vector machine (SVM) has been derived from statistical learning theory. SVM has already been marked as a novel development by learning from examples based on polynomial function, neural networks, radial basis function, splines and other functions. The performance of each classifier is decided by classification rate (CR). Our result confirms the classification ability of LS-SVM technique is much better to classify gender from ECG signal analysis in terms of classification rate than SVM.

Keywords  ECG, HRV, SVM, LS-SVM, CR

1. Introduction

Gender is almost its most salient feature, and gender classification according to ECG is one of the most challenging problems in person identification in Biometrics[1]. Compared with other research topics in Biometrics, the academic researches on gender classification is less. In reality, successful gender classification will boost the performance of Patient recognition in large Medical database.

From last two decades It was observed that a variety of prediction models have been proposed in the machine learning that include time series models, regression models, adaptive neuro-fuzzy inference systems (ANFIS), artificial neural network (ANN) models and SVM models[2]. Due to the effectiveness and smoothness of ANN model, it is widely used in various fields like pattern recognition, regression and classification. For classification and non-linear function estimation, the recently proposed SVM technique is an innovative kind of machine learning method introduced by Vapnik and co-workers[3, 4, 5]. This method is further enhanced by various investigators for different applications like classification, feature extraction, clustering, data reduction and regression in different disciplines. SVM have remarkable generalization performance and many more advantages over other methods, and hence SVM has attracted attention and gained extensive application. Suykens and his group[6] have proposed the use of LS-SVM for simplification of traditional of SVM. Apart from its use in classification in various areas of pattern recognition, it has been extensively used in handling regression problems successfully[7, 8]. In LS-SVM, a set of only linear equation (Linear programming) is solved which is much easier and computationally more simple which made it advantageous than SVM.

In the present study, both SVM and LS-SVM classifiers have been designed, trained and tested using various kernel functions like linear and (Radial Basic Function) RBF kernel. RBF kernel LS-SVM gives better performance in terms of classification rate among other classifiers.

2. Materials and Methods

Figure 1. Custom made ECG device
In this current study, the ECG of different people was recorded. An in-house developed ECG data acquisition system was used for this study. The ECG system mainly composed of two parts, viz. ECG electrodes and ECG-DAQ. ECG-DAQ, a USB-based device, helped in recording ECG signals in PC. Figure 1 shows the ECG device connected with PC which was used for data recording in our study.

Biomedical Starter Kit from National Instrument software was used to extract the different time and frequency domain features of HRV (e.g. mean heart rate (HR), mean RR, Mean NN, standard deviation of RR intervals (SDNN), root mean square of successive difference (RMSSD), NN50, pNN50 and SD1 and SD2 of Poincare plot). The HRV features were then analysed by non-linear statistical analysis using Classification and regression trees (CART) and Boosted tree (BT) classification to determine the significant features in STATISTICA (v7) in figure 2. A combination of the features was subsequently used for Gender Classification using SVM and LS-SVM in MATLAB 10.1.

After prediction of significant features like (RR Mean, RR Standard Deviation (std.), HR mean, HR Std, root mean square of successive difference (RMSSD), NN50, pNN50, LF peak, HF Peak, LF Power, HF Power, LF/HF ratio) from CART and BT then these feature values are the input to both SVM classifier. At the output of both classifiers we will classify two classes i.e. (boy and girl). The binary values assigns to girl class as 0 and for boy class the value is 1. After classification we compare both the values in terms of Classification rate (CR).

The input data are normalized before being processed in the network as follows:

In this method of normalization, the maximum values of the input vector component are given by:

\[ n_{i,\text{max}} = \max \left(n_i(p)\right), p = 1 \ldots N_p, i = 1 \ldots N_i \]

Where \( n_i(p) \) is the input features and \( N_p \) is the number of patterns in the training set and testing set,

\[ n_{i,\text{nor}}(p) = \frac{n_i(p)}{n_{i,\text{max}}}, p = 1 \ldots N_p, i = 1 \ldots N_i \]

After normalization, the input variables lie in the range of 0 to 1.

### 3. SVM Classification

SVM technique is an attractive kind of machine learning method introduced by Vapnik and co-workers[3, 4, 5]. This method is further modified by various scientists for different applications like classification, feature extraction, clustering, data reduction and regression in different disciplines of engineering. Our present analysis is based on the classification of binary class data by employing SVM technique. This method builds a Hyperplane for separation of data into two classes in simple binary classification of linear separable training data vector (\( x_1, x_2, x_3, \ldots, x_n \)) in \( n \) dimensional Space. A class decision function associated with Hyperplane is weighted sum of training data set and bias value respectively. New test data according to the classification by SVM classifier is assigned to a class according to sign of decision function as:

- Testing data belongs to class-1 (male class) if \[ w^T \phi(x) + b \geq 1 \] (3.2)
- Test data belongs to class-2 (female class) if \[ w^T \phi(x) + b \leq -1 \] (3.3)

And

\[ w^T \phi(x) + b = 0 \] (3.4)

Is the decision boundary corresponding to Weight vector and bias value for optimal Hyperplane. Support vectors are obtained by maximizing the distance between the closest training point and the corresponding Hyperplane. This can be done by maximizing the margin defined as \( M = \frac{2}{||w||} \) as minimization of

\[ \frac{||w||^2}{2} \] (3.5)

Under the methodologies

\[ y_i (w^T \phi(x_i) + b) \geq 1 \] (3.6)

Different number of mathematical algorithms exists for
determining the value of weight and bias under the condition (3.5) and (3.6). One of the most efficient method used in SVM is Quadratic Optimization problem. Its solution of the problem involves construction of dual problem with the use of Lagrange multiplier $\alpha_i$ which is given as follows:

$$\sum_{i=1}^{N} \alpha_i - \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \alpha_i \alpha_j y_i y_j x_i x_j \tag{3.7}$$

The equation (3.7) is maximized under the conditions

$$\sum \alpha_i y_i = 0 \quad \text{And} \quad x_i \geq 0$$

For all value of $i = 1, 2, \ldots, N$. After solving Quadratic optimization problem, the values of weight and bias are obtained as

$$w = \sum \alpha_i y_i x_i \tag{3.8}$$

And

$$b = y_i - w^T x_i \tag{3.9}$$

Where $x_i$ is support vector for each nonzero value of $\alpha_i$. Hence, the classification function for a test data point $x$ is inner product of support vector and test data point, which is given as follows

$$y(x) = \sum \alpha_i y_i x_i^T x + b \tag{3.10}$$

SVM maps $n$-dimensional data vector into a $d$-dimensional feature space ($d>n$) with help of a mapping function for binary classification of nonlinear training data points. This Mapping function or kernel function provides a Hyperplane which separate the classes in high dimensional feature space. Using standard Quadratic Programming (QP) optimization technique, the Hyperplane maximizes the margin between classes. Those data point which are Closest to the Hyperplane are used to measure the margin and named as support vectors. In dual formulation of quadratic optimization problem instead of using dot product of training data points in high dimensional feature space, kernel trick is used. Kernel function defines the inner product of training data points in high dimensional feature space.

Thus the kernel function is defined as

$$k(x_i, x_j) = \phi^T(x_i) \phi^T(x_j) \tag{3.11}$$

The various advantages of kernel function are, It reduces the mathematical as well as the computational complexity in higher dimensional feature space. In this paper, commonly used kernel functions are linear, polynomial, radial Gaussian and sigmoid are defined as follows:

- $k(x_i, x_j) = x_i x_j$ (Linear kernel Function)
- $k(x_i, x_j) = (x_i x_j + c)^d$ (Polynomial Kernel Function)
- $k(x_i, x_j) = \frac{|x_i - x_j|^2}{2\sigma^2}$ (Radial Gaussian kernel function)
- $k(x_i, x_j) = e^{-\sigma^2}$ (Sigmoid kernel function)

For $\sigma > 0$ (Radial Gaussian kernel function)

The new classification function using kernel function is defined as follows:

$$y(x) = \sum \alpha_i y_i k(x_i, x_j) + b \tag{3.12}$$

Further, the testing data points are classified with these binary class trained model and final decision about class of data point is taken on the basis of majority voting of class. The performance of model is determined by classification rate equal to

$$(\text{CR}) = \frac{(\text{TP} + \text{FN})}{(\text{TP} + \text{TN} + \text{FP} + \text{FN})} \tag{3.13}$$

Where TP=True Positive, TN=True Negative, FP=False Positive and FN=False Negative.

4. LS-SVM Classification

The formulation of LS-SVM is introduced as follows. Given a training set $\{x_i, y_i\}_{i=1}^{N}$ with input data $x_i \in \mathbb{R}^n$ and corresponding binary class trained model and final decision about class of data point is taken on the basis of majority voting of class. The following Classification model can be constructed by using non-linear mapping function $\phi(x)$. The formulation of LS-SVM is introduced as follows.

$$y = w^T \phi(x) + b \tag{4.1}$$

$$\{ w^T \phi(x_i) + b \geq 1, \text{ if } y_i = +1 \}$$

$$\{ w^T \phi(x_i) + b \leq -1, \text{ if } y_i = -1 \}$$

Where $w$ is weight vector and $b$ is the bias term. As in LS-SVM, it is necessary to minimize a cost function $C$ containing a penalized regression error for binary target, as follows:

$$\min C(w, e) = \frac{1}{2} w^T w + \frac{1}{2} \gamma \sum_{i=1}^{N} e_i^2 \tag{4.2}$$

Subject to equality constraints

$$y_i = \phi^T(x_i) w + b + e_i, \quad i = 1, 2, \ldots, N \tag{4.3}$$

The first part of this cost function is a weight decay which is used to regularize weight sizes and penalize large weights. Due to this regularization, the weights converge to similar value. Large weights deteriorate the generalization ability of the LS-SVM because they can cause excessive variance. The second part of eq. (4.2) is the regression error for all training data. The parameter $\gamma$, which has to be optimized by the user, gives the relative weight of this part as compared to the first part. The restriction supplied by eq. (4.3) gives the definition of the regression error. To solve this optimization problem, Lagrange function is constructed as

$$L(w, b, e, \alpha) = \frac{1}{2} w^T w + \gamma \sum_{i=1}^{N} e_i^2$$

$$- \sum_{i=1}^{N} \alpha_i \{ w^T \phi(x_i) + b + e_i - y_i \} \tag{4.4}$$

Where $\alpha_i$ are the Lagrange multipliers. The solution of eq. (4.4) can be obtained by partially differentiating with respect to $w$, $b$, $e$, and $\alpha_i$

Then

$$w = \sum_{i=1}^{N} \alpha_i \phi(x_i) = \sum_{i=1}^{N} \gamma e_i \phi(x_i) \tag{4.5}$$
Where a positive definite Kernel is used as follows:

\[ K(x_i, x_j) = \phi(x_i)^T \phi(x_j) \]  

(4.6)

An important result of this approach is that the weights (w) can be written as linear combination of the Lagrange multipliers with the corresponding data training (x_i). Putting the result of eq. (4.5) into eq. (4.1), the following result is obtained as

\[ y = \sum_{i=1}^{N} \alpha_i \phi(x_i)^T \phi(x) + b \]  

(4.7)

For a point \( y_j \) to evaluate it is:

\[ y_j = \sum_{i=1}^{N} \alpha_i \phi(x_i)^T \phi(x_j) + b \]  

(4.8)

The vector follows from solving a set of linear equations:

\[ A \begin{bmatrix} \alpha \\ b \end{bmatrix} = \begin{bmatrix} y \\ 0 \end{bmatrix} \]  

(4.9)

Where A is a square matrix given by

\[ A = \begin{bmatrix} K + \frac{I}{\gamma} & 1_N \\ 1_N^T & 0 \end{bmatrix} \]  

(4.10)

Where K denotes the kernel matrix with \( i^{th} \) element in eq. (4.5) and I denotes the identity matrix \( N \times N \).

\[ 1_N = [1 \ 1 \ \ldots \ 1]^T \]

Hence the solution is given by:

\[ \begin{bmatrix} \alpha \\ b \end{bmatrix} = A^{-1} \begin{bmatrix} y \\ 0 \end{bmatrix} \]  

(4.11)

All Lagrange multipliers (the support vectors) are non-zero, which means that all training objects contribute to the solution and it can be seen from eq. (4.10) to eq. (4.11). In contrast with standard SVM the LS-SVM solution is usually not sparse. However, by pruning and reduction techniques a sparse solution can easily achieved.

Depending on the number of training data set, either an iterative solver such as conjugate gradients methods (for large data set) can be used or direct solvers, in both cases with numerically reliable methods.

In application involving nonlinear regression it is not enough to change the inner product of \( \phi(x_i), \phi(x_j) \) eq. (4.7) by a kernel function and the \( i^{th} \) element of matrix K equals to eq. (4.5).

This shows the following nonlinear regression function:

\[ y = \sum_{i=1}^{N} \alpha_i K(x_i, x) + b \]  

(4.12)

For a point \( x_j \) to be evaluated, it is:

\[ y_j = \sum_{i=1}^{N} \alpha_i K(x_i, x_j) + b \]  

(4.13)

For LS-SVM, there are lot of kernel function (Radial basis function, Linear polynomial), sigmoid, bspline, spline, etc. However, the kernel function more used is a simple Gaussian function, polynomial function and RBF. They are defined by:

\[ K(x_i, x_j) = \exp \left( -\frac{\|x_i - x_j\|^2}{\sigma_{sv}^2} \right) \]  

(4.14)

\[ K(x_i, x_j) = (x_i^T x_j + t)^d \]  

(4.15)

Where d is the polynomial degree and \( \sigma_{sv}^2 \) is the squared variance of the Gaussian function, to obtained support vector it should be optimized by user. In order to achieve a good generalization model it is very important to do a careful model selection of the tuning parameters, in combination with the regularization constant \( \gamma \).

### 4. Result and Discussion

In this study, the proposed modelling are carried out; 25 sets of input-output patterns used for training both networks and for testing purpose the remaining 12 sets are used. The software programs developed are used for implementation using MATLAB version 10.1. In the beginning, SVM network was trained with commonly used kernels like Linear and RBF Kernel Function. Table(1-2) shows the performance of model means of Percentage of Classification rates(CR) obtained from the processing of testing data with respect to SVM and LS-SVM model with RBF kernel and Linear kernel.

| True Class | Predicted Class | Class-1(Boy) | Class-2(Girl) | Classification Rate(%) |
|------------|-----------------|--------------|---------------|------------------------|
| Class-1(Boy) | 5 | 2 | 67% |
| Class-2(Girl) | 2 | 3 |        |

| True Class | Predicted Class | Class-1(Boy) | Class-2(Girl) | Classification Rate(%) |
|------------|-----------------|--------------|---------------|------------------------|
| Class-1(Boy) | 5 | 1 | 84% |
| Class-2(Girl) | 1 | 5 |        |

| True Class | Predicted Class | Class-1(Boy) | Class-2(Girl) | Classification Rate(%) |
|------------|-----------------|--------------|---------------|------------------------|
| Class-1(Boy) | 5 | 2 | 75% |
| Class-2(Girl) | 1 | 4 |        |
Table 4. Confusion matrix for Test data sheet for LS-SVM Modeling (using RBF Kernel Function)

| Predicted Class | Class-1(Boy) | Class-2(Girl) | Classification Rate(%) |
|-----------------|--------------|--------------|------------------------|
| Class-1(Boy)    | 5            | 0            | 92%                    |
| Class-2(Girl)   | 1            | 6            |                        |

5. Conclusions

This paper proposes a gender classification from ECG signal using LS-SVM and SVM technique. The different input features extracted from HRV analysis are directly feed to SVM and LSSVM classifier. Both the classifiers are designed, trained and tested. LS-SVM classifier with RBF kernel gives better classification rate of 92% among other models. This shows LS-SVM as promising results for the classification of the Gender based on HRV and ECG signal analysis.

REFERENCES

[1] Z.H Wang, Z.C Mu, “Gender classification using selected independent-features based on genetic algorithm” Proceedings of the Eighth International Conference on Machine Learning and Cybernetics, Baoding, 12-15 July 2009.

[2] W. Bartkiewicz “Neuro-fuzzy approaches to short-term electrical load forecasting”, IEEE Explorer, vol 6, pages 229-234, 2000.

[3] V. Vapnik, The Nature of Statistical Learning Theory, Springer, New York, 1995.

[4] V. Vapnik, Statistical Learning Theory, Wiley, New York, 1998.

[5] V. Vapnik, “The support vector method of function estimation, In Nonlinear Modeling: Advanced Black-box Techniques, Suykens J.A.K., Vandewalle J. (Eds.), Kluwer Academic Publishers, Boston, pp.55-85, 1998.

[6] J.A.K Suykens, T Van Gestel, J De Brabanter, B De Moor, J Vandewalle, Least Square SVM. Singapore: World Scientific, 2002.

[7] D. Hanbay, “An expert system based on least square support vector machines for diagnosis of the valvular heart disease”, Expert Systems with Application, 36(4), part-1, 8368-8374, 2009.

[8] Z Sahli, A. Mekhaldi, R. Boudissa, S. Boudrahem, “Prediction parameters of dimensioning of insulators under non-uniform contaminated condition by multiple regression analysis”, Electric Power System Research, Elsevier 2011 in press.

[9] G. Zhu, D.G Blumberg, (2001) Classification using ASTER data and SVM Algorithms: The case study of Beer Sheva, Israel, Remote Sens. of Environ., 80, 233-240.

[10] V. Kecman, (2005) Support Vector Machines: Theory and Applications Lipo Wang (Ed.) Support vector machine an introduction, Springer-Verlag Berlin Heidelberg, 1-48.

[11] V. Kecman, (2001) Learning and soft computing: Support vector machine, Neural network and Fuzzy logic models, MIT Press, Cambridge, MA, 148-176.