Critical comments on EEG sensor space dynamical connectivity analysis

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ABSTRACT

The use of electroencephalography (EEG) to study brain functioning and dynamics in humans has known a long history. Over the years, different analysis techniques have been developed and applied to EEG recordings that allow one to investigate how different brain areas interact. One particular class of methods, based on the linear parametric representation of multiple interacting time series, is widely used to study causal connectivity in the brain in both fundamental and clinical neuroscientific research. However, the results obtained by these methods should be interpreted with great care. The goal of this paper is to show, both theoretically and using simulations, that results obtained by applying causal connectivity measures on the sensor (scalp) time series do not allow interpretation in terms of interacting brain sources. Although many measures of causal connectivity derived from EEG sensor time series are affected by this, here we will focus on the well-known time domain index of Granger causality (GC) and on the frequency domain directed transfer function (DTF). Using the state-space framework and designing two different simulation studies we show that mixing effects caused by volume conduction can lead to spurious connections, detected either by time domain GC or by DTF, when interpreted in terms of anatomically interacting sources. Therefore, GC/DTF causal connectivity
measures should be computed at the source level, or derived within analysis frameworks that model the effects of volume conduction.

**Keywords**

EEG, Brain connectivity, MVAR, Granger causality, Directed transfer function

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1. **Introduction**

With the advent of non-invasive techniques such as, positron emission tomography (PET), functional magnetic resonance imaging (fMRI), electroencephalograph (EEG), magnetoencephalography (MEG) and more recently functional near-infrared spectroscopy (fNIRS), the study of the dynamical behaviour of the human brain has become a major field in science. Along with these techniques, many data analysis tools have been developed that allow researchers to investigate brain functioning to a greater extent. For many years, researchers were mostly interested in the localization of function both in space (e.g. fMRI) and time (e.g. EEG). More recently there has been a growing interest in functional integration, which refers to the interplay between functionally segregated brain areas (Friston 2011). This tendency has led to the development, refinement and use of advanced data analysis techniques such as dynamic causal modelling (DCM; Friston et al. 2003), independent component analysis (ICA, e.g. Makeig et al. 1996; Van De Ven et al. 2004), and methods based on multivariate autoregressive (MVAR) modeling. While each of these approaches has its own merits and pitfalls, here we will focus on the application of MVAR-based connectivity analysis on EEG data.

Mainly due to its close relation with the ubiquitous concept of Granger causality (GC, Granger 1969), the use of MVAR-based measures to investigate human brain connectivity has become increasingly popular in neuroscience (e.g. Ding et al. 2006; Liao et al. 2011; Porta and Faes, 2016; Seth et al. 2015). MVAR models are being extensively applied to quantify—in both time and frequency domains—the concept of GC expressing the direct causal influence from one series to another (Baccala et al. 2001; Ding et al. 2006; Seth et al. 2015), as well as the related concept of total causal influence between two time series—expressed in the frequency domain by the so-called directed transfer function (DTF; Kamiński and Blinowska 1991). Although the use of MVAR modelling on neural time series has been debated (e.g. Friston et al. 2013; Friston et al. 2014; Seth et al. 2015), this approach is widely used in neuroscience due to its high flexibility (no assumptions are made about the underlying neural
mechanisms) and easiness of implementation (the derived measures like GC and DTF are obtained from the model parameters estimated by standard least squares techniques). Moreover, there is a continuous refinement of MVAR-based methods in order to deal with issues related to applicative specific contexts. Recently, for example, linear state space (SS) models have been proposed for GC analysis, which can overcome the bias due to e.g. sampling and filtering (Barnett and Seth 2015), or account for the well know effect of volume conduction typical of EEG analysis (Cheung et al. 2010).

In this paper, we do not intend to debate the use of MVAR-based and GC analyses in neuroscience. Our goal is to show that MVAR-based analysis of causal connectivity performed at the level of EEG sensors does not allow interpretation in terms of anatomically interacting sources. There are two reasons why this interpretation is problematic. First, no inferences can be made about the anatomical location of the (possibly) interacting sources based on the location of the sensors (Nunez and Srinivasan 2006; Haufe et al. 2013; Papadopoulou et al. 2015). Secondly, since MVAR-based measures are influenced by volume conduction, their straight application to sensor EEG data can lead to the detection of spurious connections. The former problem is generally accepted in the literature. Regarding the latter, there is less consensus. This issue will be the main focus of the present work which mainly disagrees with what said in Kaminski and Blinowska (2014). In that paper the authors claim that MVAR-based measures such as the DTF are not influenced by volume conduction. Their main argument is that volume conduction is an instantaneous effect and hence cannot induce a phase shift at the sensors. This might be true, but it would be impossible by construction to tell among which regions this shifts originally occurs. Along that line on the other hand, several papers were published where the DTF was applied to the EEG sensor data to make claims regarding interacting brain sources (e.g. Wyczesany et al. 2014; Ligeza et al. 2015; Wyczesany et al. 2015). On the other hand, several authors have pointed to the adverse effects of volume conduction on sensor space connectivity analysis (Gómez-Herrero et al. 2008; Schoffelen and Gross 2009; Haufe et al. 2010; Haufe et al. 2013; Bastos and Schoffelen 2016). Vinck et al. (2015) for example showed that linearly mixed additive noise (as a consequence of e.g. volume conduction) can lead to spurious connectivity. Here we will investigate the effect of volume conduction on two of the most popular MVAR measures of causal connectivity: the time domain GC index (Geweke 1982) and the DTF (Kamiński and Blinowska 1991).

The paper is organized as follows. First, we show how brain dynamics can be modelled at the source level using MVAR models and how source activity is projected to the EEG channels (section 2.1). Then, we discuss how these dynamics can be quantified both in the time and frequency domain using GC and DTF measures (section 2.2). In section 2.3, we outline three strategies for causal connectivity analysis that can applied to EEG data: 1) the analysis performed directly on sensor data; 2) a two stage
approach where the source time series are first estimated after which the analysis is performed on these reconstructed time series; 3) the analysis performed within the state space (SS) framework. Then, we show how the first strategy can lead to spurious connectivity results (section 3). This is shown first making some theoretical considerations regarding the effects of volume conduction on causal connectivity analysis of EEG sensor time series (section 3.1), and then illustrating the issue with two simulations studies (section 3.2). In the first simulation, the adverse effect of mixing are demonstrated with a simple 'toy' model. In the second simulation study, more realistic EEG data are generated. Finally, we discuss our findings in light of the existing literature.
2. Causal Connectivity Analysis of EEG Time Series

2.1 Linear Modelling of EEG Source Interaction and Volume Conduction

The general aim of the application to neural data of methods for connectivity analysis like GC and DTF is to investigate how different functionally segregated brain areas interact with each other. In the case of the EEG, the data consists of electrical potentials which are measured using multiple electrodes that are placed at different locations of the scalp. These potentials are generally believed to originate from the summation of post-synaptic current flows that are generated by local synchronized activity of many neurons. These locally synchronized neurons are conveniently represented as a cortical dipole which we call a source (Baillet et al. 2001). Due to the propagation effect known as volume conduction, these source activations are instantly mixed resulting in electrical potentials that are measured the scalp. In this study we represent the time series of \( M \) cortical sources as realizations of the stochastic process \( S(t) = [S_1(t) \ldots S_M(t)]^T \), and the corresponding measured time series of \( L \) scalp sensors as realizations of the process \( Y(t) = [Y_1(t) \ldots Y_L(t)]^T \) (where \( t = 1, \ldots, T \) and \( T \) is the length of the realization). The dynamical interactions between the sources are modelled by means of a MVAR model (Lütkepohl 2005)

\[
S(t) = \sum_{d=1}^{p} A(d)S(t-d) + U(t) \tag{1}
\]

where \( A(d), d=1,\ldots,p \), are \( M \times M \) coefficient matrices, \( p \) is the maximum time lag that is used for quantifying the influences of past states on the current state and \( U(t) \) is a white noise innovation process with diagonal covariance matrix \( \Theta = E[U(t)U(t)^T] \). The mapping from source space to sensor space can be expressed by (Haufe et al. 2013)

\[
Y(t) = LS(t) + G(t) \tag{2}
\]

where \( G(t) = [G_1(t) \ldots G_L(t)]^T \) is the \( L \)-dimensional vector of the measurement noise superimposed to each channel and \( L \) is a \( L \times M \) lead field matrix. The columns of the lead field matrix summarize the so-called forward model for the different sources. Due to volume conduction, the sources are mixed (more specifically, linearly superimposed) and hence the lead field matrix is non-diagonal so that each source contributes to some extent to the measured scalp potentials. Assuming that different sources are
activated, the EEG channels therefore contain information from a mixture of sources.

2.2 Causal Connectivity Measures

Granger causality (GC) is a useful tool to quantify directed neural interactions in neuroscience (Porta and Faes 2016). The general principle of GC is based on predictability and temporal precedence: given two time series $S_1$ and $S_2$, respectively considered as the target and the driver, $S_2$ is said to Granger cause $S_1$ if the prediction of its current value is improved by considering the past values of $S_2$ compared to the case in which only the past value of $S_1$ are exploited for prediction (Granger 1969). When $M>2$ time series are considered, a distinction must be made between “direct” and “indirect” GC, where the former is obtained by conditioning on all the $M$-2 times-series other than the driver and the target, i.e., including all these other time series in the prediction models. The classical definition of “direct” GC from a driver series $S_j$ to a target series $S_i$ ($1 \leq i, j \leq M$) is based on linear MVAR models in the form of (1), where two models are formulated and predictability is assessed in terms of prediction error variance: the first model (i.e the “full” model) contains all time series exactly as in (1), and the predictability of the target series $S_i$ is assessed through the variance of $U_i$, $\theta_{ii}^F = E[U(t)^2]$; the second model (i.e., the “reduced” model) contains all time series except the driver $S_j$, so that the predictability of $S_i$ is now assessed from the reduced innovations $U(t)^R$ as $\theta_{ii}^R = E[U(t)^{R2}]$. Then, time domain GC (TGC) from $S_j$ to $S_i$ is quantified in its logarithmic formulation (Geweke 1982) as

$$TGC_{ij} = \ln \frac{\theta_{ii}^R}{\theta_{ii}^F}$$

The superscripts $F$ and $R$ refer to the full and reduced MVAR model respectively. From (3), it is clear that if the inclusion of the driver does not reduce the variance of the error (i.e. the denominator) of the target compared to the model without the driver (i.e. the numerator), then the ratio of the error variances will be 1 and hence GC will be zero. If the variance in the error is reduced, the ratio will be bigger than one and hence the GC values will be larger than 0. This implies the at least one of the coefficients in the $A$ matrices that relates the past values of the driver to the current value of the target is different from zero (Haufe et al. 2013).

Frequency domain measures of causal connectivity can be obtained by taking the Fourier transform of (1), yielding
\begin{align*}
S(\omega) &= \sum_{d=1}^{p} A(d) S(\omega) e^{-i2\pi d T \omega} + U(\omega) \quad (4a) \\
S(\omega) &= H(\omega) U(\omega), H(\omega) = (A M - \sum_{d=1}^{p} A(d) e^{-i2\pi d T \omega})^{-1} \quad (4b)
\end{align*}

where \(A M\) is the \(M \times M\) identity matrix, \(i = \sqrt{-1}\), and \(H(\omega)\) is that the transfer function acting as a linear filter which relates the zero mean white noise processes \(U(\omega)\) to the observed processes \(S(\omega)\). More specifically, the element \(Hj(\omega)\) is the frequency response of \(Sj\) to a zero phase unit amplitude sinusoidal chock with frequency \(\omega\) in \(Sj\). In the case of DTF, the elements of the transfer function are used to quantify in normalized terms the influence of the \(j\)-th innovation process on the \(i\)-th observed process, resulting in the definition (Kamiński et al. 2001)

\[y_{ij}(\omega)^2 = \frac{|H_{ij}(\omega)|^2}{\sum_{m=1}^{K} |H_{im}(\omega)|^2} \quad (5)\]

The DTF is classically adopted to infer in the frequency domain the total directed influence from \(Sj\) to \(Si\), i.e. the directed influence arising from both the direct and indirect causal connections between the two time series (Eichler 2006; Eichler 2012; Faes 2014). Importantly, since the DTF is based on the elements of the transfer function, one should keep in mind that the DTF measures the frequency response of one time series to a random sinusoidal chock (i.e. noise input) at another time series and not the frequency response to the time series itself. The interpretation of the DTF deviates from the GC notion and should be treated as a complementary measure of causal connectivity. If there are no interactions among the time-series and when each time-series only depends on its own past, the transfer function is a diagonal matrix and the DTF will be uniformly zero over frequencies for each time-series pair. If, on the contrary, there is at least one interaction among a pair of the time-series, then at least one of the off-diagonal elements in one of the \(A(d)\) matrices is non-zero and hence the transfer function \(H(\omega)\) will be a non-diagonal matrix, leading to a DTF which is not uniformly zero over the frequency range for at least one pair of channels.

2.3 Assessment of Causal Connectivity for EEG time series

In the assessment of directional coupling among different neural sources by means of GC and DTF
analyses, it is clear that the goal is to make inferences on the interactions between the source time series $S_t$. A major issue in this case is that the source time series are not directly observable, and therefore the methods presented above cannot be applied in a straightforward way. Three possible approaches can be followed in this case, as discussed in the following.

The first approach is to perform causal connectivity analysis as described in Sect. 2.2 directly on the available sensor time series $Y(t)$ (Kaminski and Blinowska 2014; Wyczesany et al. 2014; Wyczesany et al. 2015). This implies considering the MVAR model

$$Y(t) = \sum_{d=1}^{P} \tilde{A}(d)Y(t - d) + \tilde{U}_t(t).$$

which, being estimated from different time series than the sources $S(t)$, will in general yield MVAR parameters ($\tilde{A}(d), \tilde{\theta}$) that differ from those relevant to the interacting ($A(d), \theta$), sources and thus will lead to different values of GC and DTF.

The second way to proceed is to employ a two-stage approach, by (i) reconstructing the time course of the neural sources by means of some source reconstruction method (e.g. Michel et al. 2004) to get the time series $\tilde{S}(t) = [\tilde{S}_1(t) \cdots \tilde{S}_M(t)]^T$ which represent an estimate of the unmeasured sources $S(t)$; and (ii) performing causal connectivity analysis on the reconstructed sources after identification of the MVAR model:

$$\tilde{S}(t) = \sum_{d=1}^{P} \tilde{A}(d)\tilde{S}(t) + \tilde{U}(t).$$

In this case it is expected that, if the reconstruction method and the MVAR estimation approach are accurate enough, the MVAR parameters ($\tilde{A}(d), \tilde{\theta}$) will be a good estimate of the true parameters ($A(d), \theta$), and so will be the corresponding GC and DTF values.

A third possibility is to exploit the framework of state-space (SS) models to combine source interaction and volume conduction models and estimate the measures of causal connectivity within this framework (Cheung et al. 2010; Barnett and Seth 2015). The general linear time-invariant SS model can be formulated as

$$X(t + 1) = BX(t) + W(t)$$

$$Y(t) = CX(t) + V(t).$$
where $X(t)$ is an $K$-dimensional unobserved state process, $Y(t)$ the $L$-dimensional observed process, the $K \times K$ state transition matrix $\mathbf{B}$ describes the update of the hidden states at each discrete time increment, and the $L \times K$ observation matrix $\mathbf{C}$ describes the instantaneous mapping of the state process $X$ to the observed process $Y$; $W(t)$ (state-equation error) and $V(t)$ (measurement equation error) are zero-mean white noise processes with covariances $\mathbf{\Phi} = E[W(t)W(t)^T]$ and $\mathbf{\Omega} = E[V(t)V(t)^T]$, and cross-covariance $\mathbf{\Sigma} = E[W(t)V(t)^T]$. The source interaction and volume conduction models of Eqs. (1,2) can be re-written in SS form by defining the state process $X = [S(t)^T \cdots S(t-p)^T]^T$ of dimension $K=Mp$, defining the state and observation errors $W(t) = [U(t+1)^T \cdots 0]^T$ and $V(t) = G(t)$, letting the state and measurement errors be uncorrelated ($\mathbf{\Sigma} = 0$), and setting the parameters of the state and observation equations (8a,b) as:

$$
\mathbf{B} = 
\begin{bmatrix}
A(1) & \cdots & A(p-1) & A(p) \\
I_M & \cdots & 0_M & 0_M \\
\vdots & \ddots & \vdots & \vdots \\
0_M & \cdots & I_M & 0_M
\end{bmatrix},
$$

$$
\mathbf{C} = [L, 0_{L \times (K-M)}].
$$

An important property of the SS representation is that it allows to compute the time domain measure of GC directly from the model parameters, without the need of identifying the reduced model and estimate its prediction error variance (Barnett and Seth 2015). Indeed, time domain GC among the sources is assessed in a straightforward way deriving the parameters $(\mathbf{A}_d, \mathbf{\Theta})$ from $\mathbf{B}$ and $\mathbf{\Omega}$; GC among the sensors is assessed in the time domain from the “innovations form” representation of the SS model. In the frequency domain, the DTF is computed from the moving-average representation of the SS model, which can be easily derived from the original MV AR parameters (see, e.g., Barnett and Seth 2015, for a detailed description of the procedure).

### 3. Effect of Volume Conduction on Sensor-Space Causal Connectivity

#### 3.1 Theoretical Considerations

The easiest way to accomplish causal connectivity analysis on EEG datasets is to follow the first approach described in Sect. 2.3 (Eq. (6)), since it only requires the application of MV AR modelling routines on the observed sensor time series. However, in this case simplicity comes at a price. First of all, if one finds significant GC or DTF among pairs of sensors, one cannot make inferences about the spatial location of the underlying sources except for the (rare) case when one knows (or assumes) that
the activity of one single source is express at only one EEG channel and that one knows where these source are a priori (Papadopoulou et al. 2015). If one cannot make these assumptions, the channel time series are a mixture of activated sources and therefore it is impossible to infer which source's past values that are expressed in the assigned driver sensor contribute to the prediction of another source's future which is expressed in the target sensor. Even when there are no interacting sources, a significant interaction between two sensors can be found applying standard connectivity analysis either in the time domain (e.g., the TGC index (3)) or in the frequency domain (e.g., the DTF (5)). This latter point has been recently debated (Kaminski and Blinowska 2014). In that paper, the authors claim the DTF is not influenced by volume conduction. If this would be true, then non interacting VAR sources should not lead to a significant DTF at some frequencies between any pair of sensors. However, if the sources can be expressed by (1), combined with (2) to obtain the scalp potentials, we obtain the following relations for the time and frequency domain representations of the sensor series:

\[
Y(t) = L \left( \sum_{d=1}^{P} A(d)S(t - d) + U(t) \right) + G(t) \quad (10a)
\]

\[
Y(\omega) = LH(\omega)U(\omega) + G(\omega) \quad (10b)
\]

In case of non-interacting VAR sources, the coefficient matrix \( A \) and the transfer function matrix \( H(\omega) \) are both diagonal matrices. However, given that the lead field matrix \( L \) is non-diagonal, the products \( LA(d) \) in (10a) and \( LH(\omega) \) in (10b) result in a non-diagonal matrix. This implies that the sensors can be expressed as a weighted sum of past values of all the sources (though in practice the contribution of some specific sources to a specific EEG channel can be negligible). In addition, the mixing of the sources is different for each sensor. This implies that the past values of the sensors will improve the prediction of another sensor current state (even though the mixing is instantaneous, past values are also instantaneous mixtures of sources) and hence, spurious causal connectivity will occur both when measured by the TGC (non-diagonal coefficient matrix) and when measured by the DTF (non-diagonal transfer function). Note that mixing of pure random statistically independent noise time series will not result in spurious connectivity.

3.2 Simulation I: Theoretical Connectivity Analysis of Uncoupled Sources

In this section we report the analysis of GC in both time and frequency domains for a simple theoretical example demonstrating how spurious connectivity can be measured in the sensor space as a
result of volume conduction. Specifically, we consider the case of two non-interacting sources described by the following MVAR process of order 2:

\[
\begin{align*}
S_1(t) &= 0.95S_1(t-1) - 0.70S_1(t-2) + W_1(t) \\
S_2(t) &= 0.50S_2(t-1) - 0.90S_2(t-2) + W_2(t)
\end{align*}
\] (11)

where the innovations \(W_1(t)\) and \(W_2(t)\) are independently drawn from the Gaussian distribution with zero mean and unit variance. Then, mixed time series representative of the sensor activity are obtained by pre-multiplying \(S(t) = [S_1(t) \; S_2(t)]^T\) with the following mixing matrix

\[
L = \begin{bmatrix} 0.8 & 0.3 \\ 0.4 & 0.7 \end{bmatrix}
\]

and considering zero measurement noise, i.e., \(Y(t) = L \; S(t)\).

Then, the derivations in Sect 2.3 are exploited to define the SS model descriptive of this parameter setting, and connectivity analysis is performed in both time and frequency domains computing the TGC and DTF measures from the SS representation. The TGC is zero along both directions between the two sources \(S_1\) and \(S_2\) (\(TGC_{12} = TGC_{21} = 0\)), while it results substantially larger than zero between the two sensors \(Y_1\) and \(Y_2\) (\(TGC_{12} = 0.1064, \; TGC_{21} = 0.1417\)). The profiles of the DTF obtained between the two original and mixed sources are shown in Fig. 1 together with the corresponding spectral density functions. These results of both time and frequency domain analysis show no interactions among the original source time series. On the other hand, the mixed sources reveal a clear bidirectional interaction detected by significant TGC and DTF values along the two directions of interaction.

3.2 Simulation II: Connectivity Analysis of a Realistic Pseudo-EEG dataset

This second simulation was aimed at showing the effects of volume conduction on realistic pseudo-EEG data generated using an adapted version of the simulation framework proposed by Haufe and Ewald (2016). Here, we generated three sources with only one unidirectional coupling between two sources. The MVAR model of the sources was:

\[
\begin{align*}
S_1(t) &= 0.55S_1(t-1) - 0.80S_1(t-2) + W_1(t) \\
S_2(t) &= 0.7S_2(t-1) - 0.55S_2(t-2) + 0.60S_1(t-1) + W_2(t), \\
S_3(t) &= 1.1S_3(t-1) - 0.50S_3(t-2) + W_3(t)
\end{align*}
\] (12)
with noise terms drawn again from the Gaussian distribution with zero mean and unit variance. We see that the first source ($S_1$) Granger-causes the second source ($S_2$). The third source ($S_3$) is not connected to the first two sources.

![Fig. 1 DTF analysis for simulation I, showing the profiles of DTF (off diagonal plots) and of the power spectrum (diagonal plots) of two non-interacting VAR sources before (green) and after (red) linear mixing. The simulated sampling frequency is 128 Hz.](image)

First, we generated a realization of the three sources lasting $T=100000$ points, and computed the TGC and DTF over this realization from the MVAR parameters estimated according to the standard least squares approach (Faes et al. 2012). While the DTF was obtained straightforwardly as described in Sect. 2.2 from the MVAR parameters, the TGC was computed from the SS representation of the estimated MVAR parameters, thus avoiding the fit of full and reduced MVAR models (Barnett and Seth 2015). The TGC values were: $TGC_{12} = TGC_{13} = TGC_{23} = TGC_{31} = TGC_{32} = 0$ and $TGC_{21} = 0.497$. The
DTF profiles are shown in Fig. 2.

Fig. 2 The DTF for the generated sources are shown. The diagonal panels show the power spectrum of the three sources.

Next, each of the three simulated sources was assigned to a specific anatomical location: Source one was assigned to the right occipital cortex (vertex MNI coordinates: [29 -89 4]), source two was assigned to the right middle orbital frontal cortex (vertex MNI coordinates: [41 52 -8], and the third source was assigned to the right superior temporal cortex (vertex MNI coordinates: [45 -15 3]), see fig. 3.

In addition to these three sources, 500 mutually statistically independent pink noise sources (i.e. brain noise) were generated and each brain noise source was randomly allocated to 1 of the vertices of the source model. All the generated sources were assumed to be dipoles perpendicularly oriented toward the surface. Here the ICBM-NY head combined with the finite element method (FEM) was
used to solve the forward problem (i.e. projecting source space time series to channel space time series using the lead field matrix, Haufe et al. 2015). The sources were projected to 108 EEG channels defined in 10-5 electrode placement system (Oostenveld and Praamstra 2001). Finally, random white noise was added to the channels (see Haufe and Ewald 2016 for more details about SNR and the head model). The following channels were selected for connectivity analysis in the sensor space: AF8, O2 and T8. These channels were selected as those being the closest to the three source locations. Finally, we applied eLORETA to the channel time series to recover the sources time series at the a priori defined anatomical location (Pascual-Marqui 2007). DTF calculations were also applied to the reconstructed source time series. The TGC values for the sensor-space and source reconstructed analysis can be found in table 1. The results for the sensor-space and source-reconstructed DTF analysis can be found in fig. 4A and 4B respectively. The sensor-space DTF analysis reveals a large DTF from O2 to AF8 and from O2 to T8. The DTF for the other connections are much smaller. The trends of DTF for the source-reconstructed time series were almost identical to those of the originally generated time-series.

Fig. 3 Anatomical locations of the three generated sources (red dots). The arrow indicates the unidirectional connection from source one to source two

4. Discussion

The main objective of this study was to show that the use of traditional MVAR-based connectivity analysis, yielding classic measures such as the GC in the time domain and the DTF in the frequency domain, does not allow interpretation of anatomically interacting brain areas when performed on EEG sensor-space. First of all, due to volume conduction there is no one-to-one relation between the EEG channel time series and source activity. More specifically, multiple spatially distinct neural sources
contribute to the measured EEG scalp potentials. Therefore the spatial location of the EEG channels cannot be seen as an approximation of a source's anatomical locations (such as the anatomical location underneath the electrode). Secondly, we show that, since the EEG time series are a mixture of sources

|               | Sensor-space analysis | Source reconstructed analysis |
|---------------|-----------------------|-------------------------------|
| Driver channel|                       |                               |
| Target channel| O2    | 0.0560 | 0.0404 | S1   | 0.0008 | 0.0003 |
|               | AF8   | 0.3026 | 0.0706 | S2   | 0.4800 | 0.0001 |
|               | T8    | 0.0595 | 0.0128 | S3   | 0.0017 | 0.0003 |

Table 1 Values of sensor-space and source-reconstructed TGC

spurious connectivity can occur quite easily between pairs of channels even in the absence of any causal interaction at the source level. Since the latter has been debated in the past by Kaminski and Blinowska (2014), this issue is the main focus of this paper. More specifically, the authors claim that the DTF is not influenced by volume conduction. Volume conduction in EEG is mathematically equivalent to a linear superposition (mixing) of brain sources. If the time evolution of one or more sources can be characterized by a VAR model, then the mixed time series will also contain an autoregressive component. However, since the mixing of sources is not identical for the different channels, the inclusion of past values of another (driver) channel can improve the prediction of another (target) channels' current state. The same argument was given in (Haufe et al. 2013). In that paper, the authors state that the even in the case only one MVAR source is active, the inclusion of some channels' past values will improve the prediction of the current state in another channel because both channels measure the same source but with different noise realizations (i.e. measurement noise). Crucial in their argument is the measurement noise. In case of no measurement noise, the two channels will be differently scaled versions of that source. In that case, the inclusion of the other channels' past value would be completely redundant. Viewing the MVAR model as a special case of the general linear model, the rank of the design matrix would be smaller than the number columns and hence no unique
Fig. 4 Results of causal connectivity analysis showing DTF and power spectra (on the diagonal) computed for sensor space analysis (a) and source reconstructed analysis (b)
solution would exist for the model parameter. From a practical perspective, due to numerical inaccuracies and differences in algorithms, estimates of the $A$ matrix (and hence the transfer function matrix $H$ as well) will be highly unstable (very different solutions or no-solution depending on the algorithm). The adverse effect of additive noise (and more specifically linearly mixed additive noise) on GC-based connectivity analysis was also show by (Vinck et al. 2015)

In case of multiple non-interacting MVAR sources, differentially mixing of these sources will also result in spurious connections even in the absence of additive measurement noise. In this case the inclusion of another channel past values in the model will not introduce redundancy. This was shown in the first simulation where two non-interacting MVAR sources were specified and then differentially mixed to obtain two mixed time-series. No measurement noise was added to the mixed time series. The DTF was calculated on both the original and the mixed time series. In fig. 1, one can clearly see that, although the DTF for the original sources is uniformly zero over frequencies in both directions, the DTF of the mixed times-series clearly show a bidirectional interaction. Based on the second simulation study, if one would interpret the channel DTF in terms of interacting anatomical sources, then one would conclude that the occipital cortex has a causal influence on orbital frontal cortex but also the temporal cortex while in fact only the former is true. Kaminski and Blinowska (2014), however, claim that the DTF is insensitive to volume conduction. They argue that the linear superposition of the sources is instantaneous and hence cannot produce a phase difference at the sensors. This is only true in the rare case when the phases of the sources are the same or when the power of one source is negligible compared to the other source. If there is a phase difference between two sources (which is by no means indicative of a causal interaction between these two sources), then differentially mixing of these sources to two channels, can (in theory) result in the same phase difference but also in a different phase difference and even in a no-phase difference (when the relative contribution of the sources to the channels is the same up a multiplicative constant) between two channels. Hence, linear superposition can cause a phase difference at the sensors. In short, the instantaneousness property of volume conduction cannot be used as an argument to claim the ‘insensitivity of the DTF to volume conduction’; of course, the same holds for any other measure of causal connectivity computed in the time domain (e.g., the TGC studied here) or in the frequency domain (e.g., the partial directed coherence (Baccala et al. 2001)).

Furthermore, Kaminski and Blinowska (2014) suggest that no preprocessing of the channels should be done to reduce the volume conduction effect because these procedures would destroy the causal information between sources. In our second simulation study, we show that (in principle) applying the DTF to source reconstructed time-series resulted in the correct recovery of the original (anatomical)
causal structure of the dynamical system. It should be noted that in our simulations, we used the same head model for source reconstruction and the time series were obtained at the a priori spatial locations. In practice, however, the head model can only be an approximation of the 'true' head model. It has been shown that errors in the head model can result in errors in source-space GC based connectivity analysis (Cho et al. 2015). In addition, the true locations of activated sources are not known a priori and hence need to be chosen based on the data itself or a priori knowledge (e.g. from fMRI studies using a similar paradigm; see e.g. Schoffelen and Gross (2009) for selection strategies of sources in the context of source connectivity analysis). Since source-space causal connectivity analysis requires estimates of the source time series, a source reconstruction algorithm needs to be applied to the data. Since the inverse problem is ill-posed, the solution depends on (biologically) informed constraints. Different inverse solutions pose different constraints and the accuracy of the output of the algorithm depends on the correctness of these constraints. Furthermore, inverse solution does not undo the mixing completely and hence spatial leakage will still be present. This is especially the case when the sources are close to each other. Therefore, other measures that are more robust to mixing are required to assess brain interaction even at the source level (Haufe and Ewald 2016). In sum, even though source-space causal connectivity analysis is a promising avenue, many issue still needs to be addressed in future research.

Another possibility is to use the SS framework to assess causal interactions among neural sources. When using SS models for EEG, both volume conduction and the temporal evolution of the neural state are modeled within the same framework. The SS framework has, for example, been used to solve the dynamic inverse solution in EEG, which results in better spatiotemporal recovery of the hidden neural sources (Galka et al. 2004; Yamashita et al. 2004). In the context of causal connectivity, Cheung et al. (2010), recently developed an expectation maximization algorithm to obtain model parameter of (8a) and (8b). In that algorithm, the anatomical locations of the sources needs to be specified a priori and hence prior knowledge or EEG source imaging needs to be applied first. Nevertheless, the authors showed that GC analysis using SS models was less sensitive to noise compared to the two-stage procedure. In addition, other issues (such as downsampling and other preprocessing procedures) with respect to the MVAR modelling in causal connectivity analysis can be overcome by using the SS framework (see Barnett and Seth 2015).

To conclude, sensor-space causal connectivity analysis, performed either in time or frequency domains, does not allow interpretation in terms of interacting brain sources. The measures of GC and DTF should be computed at the source level, or implemented within analysis frameworks that model the effects of volume conduction.
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