Learning interpretable disease self-representations for drug repositioning

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Abstract

Drug repositioning is an attractive cost-efficient strategy for the development of treatments for human diseases. Here, we propose an interpretable model that learns disease self-representations for drug repositioning. Our self-representation model represents each disease as a linear combination of a few other diseases. We enforce the proximity between diseases to preserve the geometric structure of the human phenome network — a domain-specific knowledge that naturally adds relational inductive bias to the disease self-representations. We prove that our method is globally optimal and show results outperforming state-of-the-art drug repositioning approaches. We further show that the disease self-representations are biologically interpretable.

1 Introduction

New drug discovery and development presents several challenges including high attrition rates, long development times, and substantial costs [Ashburn and Thor, 2004]. Drug repositioning, the process of finding new therapeutic indications for already marketed drugs, has emerged as a promising alternative to new drug development. It involves the use of de-risked compounds in human, which translates to lower development costs and shorter development times [Pushpakom et al., 2018].

A wide range of computational approaches has been proposed to predict novel indications for existing drugs. The common assumption underlying these methods is that there is biological or pharmacological relational information between drugs, e.g. chemical structure, and between diseases, e.g. disease phenotypes, that can be exploited for the prediction task. Current methods typically rely on well-defined heuristics and/or hand-crafted features. For instance, the PREDICT [Gottlieb et al., 2011] model extract drug-disease features from multiple similarity measures, and then trains a logistic regression classifier to predict novel drug indications. Similarly, [Napolitano et al., 2013] obtain features from heterogeneous drug similarity measures and then trains an SVM classifier to predict therapeutic indications of drugs. Other approaches include random walks on bipartite networks [Luo et al., 2016], and low-rank matrix completion-based approaches [Luo et al., 2018].

In this paper, we propose a self-representation learning model for drug repositioning that is able to overcome the limitations of heuristic-based approaches and extend the expressiveness of low-rank factorisation models for matrix completion. Our model builds upon the recent development of high-rank matrix completion based on self-expressive models (SEM) [Elhamifar, 2016], as well as the recent trend of deep learning on graphs [Bronstein et al., 2017, Monti et al., 2017, Hamilton et al., 2017]. We propose a geometric SEM model that integrates relational inductive bias about

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We shall prove that the cost function $Q$ where

$$\|C\|_F^2 + \frac{\beta}{2}\|C\|_F^2 + \lambda\|C\|_1 + \frac{\alpha}{2}\|C\|_{D,G}^2 + \gamma\text{Tr}(C)$$

To minimise Eq. 1, we develop an efficient multiplicative learning algorithm with theoretical guarantees of convergence. Our algorithm consists in iteratively applying the following rule:

$$c_{ij} \leftarrow c_{ij} \frac{(X^TX + \alpha CW)_{ij}}{(X^TX + \alpha CD + \beta C + \lambda I)_{ij}}$$

We shall prove that the cost function $Q(C)$ is convex and therefore, our multiplicative rule in Eq. 3 converges to a global minimum.
Although PREDICT integrates information from seven heterogeneous similarity measures, it performs poorly with high data imbalance, where a simple SEM model, which does not use any relational information between diseases, we also optimised a threshold parameter \( \tau \) for the performance of our method against PREDICT \cite{Gottlieb2011}, a recent low-rank matrix completion model called Drug Repositioning Recommendation System (DRRS) \cite{Luo2018} and a non-geometric version of our model (with \( \alpha = 0 \), SEM). For both PREDICT and DRRS, we ran the algorithms with their respective similarity measures used in the original papers. An object-oriented implementation of our model, along with datasets to reproduce our study, is available at https://github.com/Noired/GSEM.git.

### Performance Evaluation

Figure 4 summarises the performance of the methods. We observed that while GSEM is only marginally better than DRRS and PREDICT in the balanced scenario (negative-to-positive ratio 1:1, AUPRC of 0.950 ± 0.010 for GSEM, 0.947 ± 0.012 for DRRS and 0.932 ± 0.020 for PREDICT), it greatly outperforms these competitors in imbalanced scenarios (by 1.0-13.16% at 10:1, 4.67-29.15% at 30:1, 6.48-27.60% at 50:1 and 10.31-33.12% at 100:1). Although PREDICT integrates information from seven heterogeneous similarity measures, it performs poorly with high data imbalance, where, a simple SEM model, which does not use any relational prior between diseases, intrinsically outperforms PREDICT and DRRS by 1.93-23.05% at 50:1 and 6.03-28.84% at 100:1. This means that our high-rank model of \( X \) based on self-representations is able to better exploit the intrinsic relationships between diseases inferred from the data matrix \( X \) — we checked that indeed the matrix \( X \) has a high-rank (\( \text{rank} = 238/313 \)). The contribution of the relational information between diseases becomes clear when comparing the performances of the
GSEM versus SEM model: on average, GSEM outperforms SEM by 4.85% AUPRC across all the ratios.

Figure 1: (a) Drug repositioning performance. Mean and standard deviation for AUPR metric computed using ten-fold cross-validation for varying values of negative to positive label ratios \((\text{ratio} \in \{1, 5, 10, 15, 20, 30, 40, 50, 100\})\). Performance of our method (GSEM) is reported, along with that of the state-of-the-art DRRS [Luo et al., 2018], PREDICT [Gottlieb et al., 2011] and standard SEM. Our model performs best in the more realistic unbalanced scenario. (b) Model interpretation. Comparative violin plot of disease self-representation similarities. Diseases were grouped by well-known phenotypic classes. Significance levels between the average intra-class similarities for GSEM and SEM is indicated with asterisks \((p \leq 0.001, * * *)\).

4 Model Interpretation

The effectiveness of our model at predicting new disease indications for drugs prompted us to analyse whether the disease self-representations are informative of the biology underlying drug activity. We assessed model interpretability by exploring the extent to which disease self-representations were related to well-known disease classes. We retrieved disease classes from the International Classification of Diseases of the World Health Organization (WHO) (ICD10CM [WHO, 2016]). We only kept diseases belonging to a unique class, and filtered diseases belonging to a class with less than 5 diseases. For 182 diseases, we obtained 11 distinct classes (see Supplementary Materials). We then defined a disease-disease similarity as the cosine similarity of the rows of \(S = (C + C^T)/2\). For these experiments, we trained our model using all the available data in \(X\) and fixed optimal hyper-parameters (see Supplementary Material). Figure 1(b) shows the violin plots of the distribution of similarities for diseases belonging to the same class (intra-class) versus diseases belonging to distinct classes (inter-class), for both GSEM and SEM. We observed that for both GSEM and SEM, the intra-class similarity is significantly higher than the inter-class similarity (Wilcoxon Sum Rank Significance, \(p < 3.62 \times 10^{-107}\) and \(p < 3.55 \times 10^{-249}\) for SEM and GSEM, respectively), meaning that both models learn biologically meaningful self-representations for diseases. However, the intra-class disease self-representation similarity is significantly higher for GSEM than for SEM (Wilcoxon Sum Rank Significance, \(p < 1.23 \times 10^{-174}\)), suggesting that our geometric model efficiently integrates the relational phenotypic information between diseases encoded in the human phenome network.

5 Conclusions and Future Work

Inherently interpretable models are critical for applications involving high-stakes decisions such as health care [Rudin 2019]. These are unfeasible to achieve with neural nets, because the learned representations depend on uninterpreted features in other layers [Hinton 2018]. Here we proposed an inherently interpretable model, GSEM, that learns self-representations for diseases. Our model effectively integrates the relational inductive bias from the human phenome network [Van Driel et al., 2006] — better results could possibly be achieved using the [Caniza et al., 2015] disease similarity,
which has shown to be effective for the prediction of genes associated to genetic diseases [Cáceres and Paccanaro, 2019]. Ongoing research includes the integration of relational inductive bias for drugs, which implies imposing Dirichlet graph regularisation constraints on the rows of $X$.

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7 Supplementary Material

7.1 Model Implementation

**PREDICT** We re-implemented the PREDICT algorithm in Python 3.6. We computed seven drug-disease features using the original data and following the procedure in [Gottlieb et al., 2011]. To train the model, we used the `LogisticRegression` classifier from `sklearn.linear_model` to obtain the scores for the drug-disease pairs.

**DRRS** To run Drug Repositioning Recommender System [Luo et al., 2018], we used the data and code provided in the original publication. DRRS uses two complementary information for the prediction: the 2D Tanimoto chemical similarity for drugs and phenotype similarities for diseases obtained from MimMiner [Van Driel et al., 2006].

**GSEM** We implemented our proposed algorithm in Python 3.6. As model learning is based on a multiplicative learning rule similar to that of non-negative matrix factorisation (NMF) [Lee and Seung, 1999, 2001], we followed the recommended guidelines in [Berry et al., 2007] to implement it: (i) $C$ was initialised with weights sampled from a uniform distribution between $[0, b)$, with $b = 1 \times 10^{-2}$; (ii) a small value $\varepsilon \approx 1 \times 10^{-16}$ was added to the denominator of the learning algorithm to prevent division by zero. The learning rule is iteratively applied until either of the following stopping condition is met: (i) $\text{maxiter}$ iterations are completed; (ii) the relative change $\delta^{(t)}$ in the value of $C$ across two subsequent iterations is smaller than a predefined termination tolerance $\text{tol}$ [Kearfott and Walster, 2000]:

$$
\delta^{(t)} = \max \left( \frac{|c_{ij}^{(t+1)} - c_{ij}^{(t)}|}{\max_{(i,j)}|c_{ij}^{(t)}| + \varepsilon} \right) < \text{tol}
$$

SEM was naturally obtained as a special case of GSEM by setting $\alpha = 0.0$.

7.2 Experimental Details

7.2.1 Hyperparameter Tuning

GSEM hyperparameters were tuned within the grid $\alpha, \beta, \lambda \in \{0.0, 0.01, 0.1, 1.0, 10.0, 100.0\}$, $\tau \in \{0.0, 0.25, 0.65, 0.75, 0.85, 0.95\}$, with ten-fold cross-validation on the 2:1 negative-to-positive ratio setting, the one originally considered in [Gottlieb et al., 2011]. Hyperparameters for SEM were chosen likewise.

Hyperparameters optimizing average performance on validation folds were estimated to be $\alpha = 1.0, \beta = 0.1, \lambda = 0.0, \tau = 0.25$ for GSEM and $\beta = 10.0, \lambda = 0.0$ for SEM. As for model interpretation, in order to support posterior analyses we introduced sparsity by taking the largest values of $\lambda$ not compromising model performance. Accordingly, we set $\lambda = 0.01$ for GSEM and $\lambda = 1.0$ for SEM.

Penalty with coefficient $\gamma = 10^4$ was imposed on diagonal elements in every setting, and fitting parameters were set as $\text{maxiter} = 3 \times 10^3$ and $\text{tol} = 1 \times 10^{-3}$.

7.2.2 Training and Evaluation

DRRS [Luo et al., 2018], GSEM and SEM are all matrix completion models and, as thus, the whole drug-disease association matrix is taken as input in training. At each step of cross-validation, test and validation folds were hidden by nullifying the associated positives entries. After model fitting, predictions over such fold entries were compared with ground truth values to evaluate performance.

**PREDICT** [Gottlieb et al., 2011] was learnt as a standard classification model on samples being positive and negative drug-disease associations.

[^1]: [http://bioinformatics.csu.edu.cn/resources/softs/DrugRepositioning/DRRS/index.html](http://bioinformatics.csu.edu.cn/resources/softs/DrugRepositioning/DRRS/index.html)
7.3 Model Interpretation

7.3.1 Disease Classes

We report here below in Table 1, the number of disease for each of the 11 distinct classes considered in model interpretation.

| Category                                                      | Count |
|---------------------------------------------------------------|-------|
| Diseases of the nervous system                               | 38    |
| Endocrine, nutritional and metabolic diseases                | 25    |
| Neoplasms                                                    | 25    |
| Diseases of the musculoskeletal system and connective tissue | 16    |
| Diseases of the circulatory system                           | 13    |
| Diseases of the blood-(forming) organs and certain disorders involving the immune mech. | 13    |
| Diseases of the skin and subcutaneous tissue                 | 10    |
| Diseases of the eye and adnexa                               | 9     |
| Diseases of the genitourinary system                         | 9     |
| Mental, Behavioral and Neurodevelopmental disorders          | 7     |
| Symptoms, signs and abnormal clinical and laboratory findings, not elsewhere classified | 7     |
| Diseases of the digestive system                             | 5     |
| Certain infectious and parasitic diseases                    | 5     |

7.3.2 Disease Similarity Network

Figure 2 depicts the disease network obtained via cosine similarity on the representations learnt by GSEM; here we only considered sufficiently represented classes, i.e., we did not report those associated with less than 10 diseases.

From the figure it emerges how the network presents class-consistent clustering patterns.

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Figure 2: Cosine-similarity network among disease representations learnt by GSEM. Node colour indicates disease class. The plot has been produced via Gephi [Bastian et al., 2009] with ForceAtlas embedding.

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