Abstract—We propose a data-driven method for synthesizing
static analyses to detect side-channel information leaks in
cryptographic software. Compared to the conventional way
of manually crafting such static analyzers, which can be tedious,
error prone and suboptimal, our learning-based technique is not
only automated but also provably sound. Our analyzer consists
of a set of type-inference rules learned from the training data,
i.e., example code snippets annotated with the ground truth.
Internally, we use syntax-guided synthesis (SyGuS) to generate
new recursive features and decision tree learning (DTL) to
generate analysis rules based on these features. We guarantee
soundness by proving each learned analysis rule via a technique
called query containment checking. We have implemented our
technique in the LLVM compiler and used it to detect power side
channels in C programs that implement cryptographic protocols.
Our results show that, in addition to being automated and
provably sound during synthesis, our analyzer can achieve the
same empirical accuracy as two state-of-the-art, manually-crafted
analyzers while being 300X and 900X faster, respectively.

I. INTRODUCTION

Static analyses are being increasingly used to detect security
vulnerabilities such as side channels [1]–[4]. However, manu-
ally crafting static analyzers to balance between accuracy
and efficiency is not an easy task: even for domain experts,
it can be labor intensive, error prone, and result in suboptimal
implementations. For example, we may be tempted to add
expensive analysis rules for specific sanitized patterns without
realizing they are rare in target programs. Even if the analysis
rules are carefully tuned to a corpus of code initially, they are
unresponsive to changing characteristics of the target programs
and thus may become suboptimal over time; manually updat-
ing them to keep up with new programs would be difficult.

One way to make better accuracy-efficiency trade-offs and
to dynamically respond to the distribution of target programs
is to use data-driven approaches [5], [6] that automatically
synthesize analyses from labeled examples provided by the
user. However, checking soundness or compliance with user in-
tent (generalization) has always formed a significant challenge
for example-based synthesis techniques [7]–[11]. The lack of
soundness guarantees, in particular, hinders the application of
such learned analyzers in security-critical applications. While
several existing works [12]–[15] try to address this problem,
rigorous soundness guarantees have remained elusive.

To overcome this problem, we propose a learning-based
method for synthesizing a provably-sound static analyzer that
detects side channels in cryptographic software, by inferring a
distribution type for each program variable that indicates if its
value is statistically dependent on the secret. The overall flow
of our method, named GPS, is shown in Fig. 1. The input is
a set of training data and the output is a learned analyzer. The
training data are small programs annotated with the ground
truth, e.g., which program variables have leaks.

Internally, GPS consists of a learner and a prover. The learner
uses syntax guided synthesis (SyGuS) to generate recursive
features and decision tree learning (DTL) to generate

type-inference rules based on these features; it returns a set
R of Datalog formulas that codify these rules. The prover
checks the soundness of each learned rule, i.e., it is not
only consistent with the training examples but also valid for
any unseen programs. This is formulated by solving a query
containment checking problem, i.e., each rule must be justified
by existing proof rules called the knowledge base (KB). Since
only proved rules are added to the analyzer, the analyzer is
guaranteed to be sound. If a rule cannot be proved, we add
a counter-example to prevent the learner from generating it
again.

We have implemented GPS in LLVM and evaluated its
effectiveness on 568 C programs that implement cryptographic protocols and algorithms [16]–[18]. Together, they have 2.691K lines of
C code. We compared our learned analyzer with two state-
of-the-art, hand-crafted side-channel analysis tools [1], [2].
Our experiments show that the learned analyzer achieves the
same empirical accuracy as the two state-of-the-art tools, while
being several orders-of-magnitude faster. Specifically, GPS is,
on average, 300× faster than the analyzer from [1] and 900×
faster than the analyzer from [2].

To summarize, this paper makes the following contributions:
• We propose the first data-driven method for learning
a provably sound static analyzer using syntax guided
synthesis (SyGuS) and decision tree learning (DTL).
• We guarantee soundness by formulating and solving a
Datalog query containment checking problem.
• We demonstrate the effectiveness of our method for
detecting side channels in cryptographic software.

In the remainder of this paper, we begin by presenting the
technical background in Section II and our motivating example in Section III. We then describe the learner in Section IV and the prover in Section V, followed by the experimental results in Section VI. Finally, we survey the related work in Section VII and conclude in Section VIII.

II. PRELIMINARIES

A. Power Side-Channels

Prior works in side-channel security [19]–[21] show that variance in the power consumption of a computing device may leak secret information; for example, when a secret value is stored in a physical register, its number of logical-1 bits may affect the power consumption of the CPU. Such side-channel leaks are typically mitigated by masking, e.g., using \( d \) random bits \((r_1, \ldots, r_d)\) to split a key bit into \( d + 1 \) secret shares: \( key_1 = r_1, \ldots, key_d = r_d \), and \( key_{d+1} = r_1 \oplus r_2 \ldots \oplus r_d \oplus key \), where \( \oplus \) denotes the logical operation exclusive or (XOR). Since all \( d + 1 \) shares are uniformly distributed in \([0, 1]\), in this theory, an order-d masking scheme is secure in that any combination of less than \( d \) shares cannot reveal the secret, but combining all \( d + 1 \) shares, \( key_1 \oplus key_2 \ldots \oplus key_{d+1} = key \), recovers the secret.

In practice, masking countermeasures must also be implemented properly to avoid de-randomizing any of the secret shares accidentally. Consider \( t = t_L \oplus t_R = (r_1 \oplus key) \oplus (r_1 \oplus b) = key \oplus b \). While syntactically dependent on the two randomized values \( t_L \) and \( t_R \), \( t \) is in fact leaky because, semantically, it does not depend on the random input \( r_1 \). In this work, we aim to learn a static analyzer that can soundly prove that all intermediate variables of a program that implements masking countermeasures are free of such leaks.

B. Type Systems

Type systems prove to be effective in analyzing power side channels [11], e.g., by certifying that all intermediate variables of a program are statistically independent of the secret. Typically, the program inputs are marked as public (INPUB), secret (INKEY) or random (INRAND), and then the types of all other program variables are inferred automatically.

The type of a variable \( v \), denoted \( \text{TYPE}(v) \), may be RUD, SID, or UKD. Here, RUD stands for random uniform distribution, meaning \( v \) is either a random bit or being masked by a random bit. SID stands for secret independent distribution, meaning \( v \) does not depend on the secret. While an RUD variable is, by definition, also SID, an SID variable does not have to be RUD (e.g., variables that are syntactically independent of the secret). Finally, UKD stands for unknown distribution, or potentially leaky; if the analyzer cannot prove \( v \) to be RUD or SID, then it is assumed to be UKD.

Type systems are generally designed to be sound but not necessarily complete. They are sound in that they never miss real leaks. For example, by default, they may safely assume that all variables are UKD, unless a variable is specifically elevated to SID or RUD by an analysis rule. Similarly, they may conservatively classify SID variables as UKD, or classify RUD variables as SID, without missing real leaks. In general, the sets of variables that can be marked as the three types form a hierarchy: \( S_{\text{RUD}} \subseteq S_{\text{SID}} \subseteq S_{\text{UKD}} \).

C. Relations

A program in static single assignment (SSA) format can be represented as an abstract syntax tree (AST). Static analyzers infer the type of each node \( x \) of the program’s AST based on various features of \( x \). In this work, pre-defined features are represented as relations.

- Unary relations \( \text{INPUB}(x) \), \( \text{INKEY}(x) \), and \( \text{INRAND}(x) \) denote the given security level of a program input \( x \), which may be public, secret, or random.
- Unary relations \( \text{RUD}(x), \text{SID}(x) \), and \( \text{INRAND}(x) \) denote the inferred type of a program variable \( x \), which may be uniformly random, secret independent, or unknown.
- Unary relation \( \text{OP}(x) \) denotes the operator type of the AST node \( x \), e.g., \( \text{OP}(x) \) := ANDOR \( (x) \) \( | \) XOR \( (x) \), where ANDOR \( (x) \) means that \( x \)'s operator type is either logical or and or logical and \( \text{or} \), and XOR \( (x) \) means that \( x \)'s operator type is exclusive or.
- Binary relations \( \text{LC}(x, L) \) and \( \text{RC}(x, R) \) indicate that the AST nodes \( L \) and \( R \) are the left and right operands of \( x \), respectively.
- Binary relation \( \text{supp}(x, y) \) indicates that the AST node \( y \) is used in the computation of \( x \) syntactically, while \( \text{dom}(x, y) \) indicates that random program input \( y \) is used in the computation of \( x \) semantically.

III. MOTIVATION

Consider the program in Fig. 24 which computes the \( \chi \) function from Keccak, a family of cryptographic primitives for the SHA-3 standard [22], [23]. It ultimately computes the function \( n_1 = n_1 \oplus (n_2 \land n_3) \), where \( \oplus \) means XOR. Unfortunately, a straightforward implementation could potentially leak knowledge of the secret inputs \( n_1, n_2 \) and \( n_3 \) if the attacker were able to guess the intermediate results \( \sim n_2 \) and \( \sim n_2 \land n_3 \) via the power side-channels [24], [23]. The masking countermeasures in the implementation therefore use three additional random bits \( r_1, r_2 \) and \( r_3 \) to prevent exposure of the private inputs while still computing the desired function.

A. Problem Setting

Given such a masked program, users want to determine if they succeed in eliminating side-channel vulnerabilities: in particular, if each intermediate result is uniformly distributed (RUD) or at least independent of the sensitive inputs (SID). The desired static analysis thus associates each variable \( x \) (e.g., \( n_1 \)) with the elements of a three-level abstract domain, RUD, SID or UKD, indicating that \( x \) is uniformly distributed (RUD), secret independent (SID), or unknown (UKD) and therefore potentially vulnerable.

The decision tree in Fig. 25 represents the desired static analyzer, which accurately classifies most variables of the training corpus, and is also sound when applied to new programs. Given variable \( x \), the decision tree leverages the features of \( x \)—such as the operator type of \( x \) \( (\text{OP}(x) := \text{ANDOR}(x) \mid \text{XOR}(x)) \).
user would like to synthesize. Here, \( x \) is a program variable, whose type is being computed; \( L \) and \( R \) are its left and right operands, respectively, and \( f(x) \) is a synthesized feature shown in Fig. 2a (represented by recursive Datalog program).

Fig. 2. The program on the left is a perfectly masked \( \chi \) function from MAC-Keccak. The decision tree on the right represents the static analyzer that the user would like to synthesize. Here, \( x \) is a program variable, whose type is being computed; \( L \) and \( R \) are its left and right operands, respectively, and \( f(x) \) is a synthesized feature shown in Fig. 2a (represented by recursive Datalog program).

either require computationally intensive deductive synthesis or cannot guarantee soundness and thus produce errors in both directions, including false alarms and missed bugs.

In contrast, \( GPS \) combines inductive synthesis from user annotations with logical entailment checking against a more comprehensive, known-to-be-correct set of proof rules that form the knowledge base (\( KB \)). It takes as input training programs like the one in Fig. 2a, where the labels correspond to the types of program variables (\( \text{RUD}/\text{SID}/\text{UKD} \) for intermediate results and \( \text{INRAND}/\text{INPUB}/\text{INKEY} \) for inputs). The users are free to annotate as many or as few of these types as they wish: this affects only the precision of the learned analyzer and not its soundness. Second, \( GPS \) also takes as input the knowledge base \( KB \), consisting of proof rules that describe axioms of propositional logic (Fig. 8) and properties of the distribution types (Fig. 10). In return, \( GPS \) produces as output a set of Datalog rules which simultaneously achieve high accuracy on the training data and provably sound with respect to \( KB \).

The proof rules for \( KB \) were collected from published papers on masking countermeasures \( \text{[1], [2], [16]} \). We emphasize that \( KB \) is not necessarily an executable static analyzer since repeated application of these proof rules need not necessarily reach a fixpoint and terminate in finite time; Furthermore, even in cases where it does terminate, \( KB \) may be computationally expensive and infeasible for application to large programs.

As a concrete example, we compare excerpts of the rules learned by \( GPS \) in Fig. 3a to the corresponding rules from SCInfer \( 2 \) —a human-written analysis—in Fig. 3b. LC(\( x, L \)) and RC(\( x, R \)) arises in both versions, indicating that \( L \) and \( R \) are the left and right operands of \( x \) respectively. Specifically, in Fig. 3b \( \text{supp}(x, y) \) indicates that \( y \) is used in the computation of \( x \) syntactically while \( \text{dom}(x, y) \) denotes that random variable \( y \) is used in the computation of \( x \) semantically. Observe the computationally expensive set operations in the human-written version to the simpler rules learned by \( GPS \) without loss of soundness or perceptible loss in accuracy. These points are also borne out in our experiments in Table III where
B. Feature Synthesis and Rule Learning

The learned analyzer associates each node \( x \) of a program’s abstract syntax tree (AST) with an element of the distribution type \( \{ \text{UKD}(x), \text{SID}(x), \text{RUD}(x) \} \). We may therefore interpret the analyzer as a decision tree that, by considering various features of an AST node, maps it to a type. With a pre-defined set of features, such as those shown in Fig. 4a, analyzers of this form can be learned with classical decision tree learning (DTL) algorithms. Fig. 4b shows such an analyzer, learned from the labeled program of Fig. 2a.

Unfortunately, the pre-defined features may not be strong enough to distinguish between nodes with different training labels, e.g., \( b4 \) and \( n1 \) from the training program, which have distinct labels \( \text{RUD}(b4) \) and \( \text{UKD}(n1) \), but after being sifted into the node highlighted in red in Fig. 4b, cannot be separated by any of the features from Fig. 4a. To ensure soundness, the learner would be forced to conservatively assign the label \( \text{UKD}(x) \), which sacrifices the accuracy.

\( \text{GPS} \) thus includes a feature synthesis engine, triggered whenever the learner fails to distinguish between two different labeled variables. In tandem with recursive feature synthesis, \( \text{GPS} \) overcomes the limited expressiveness of DTL by enriching syntax space to capture more desired patterns. Observe that paths of a decision tree can be represented as Datalog rules, e.g., the red path in Fig. 4b is equivalent to

\[
\text{UKD}(x) \leftarrow \text{XOR}(x) \land \text{XOR}(R) \land \text{RUD}(L) \land \text{LC}(x, L) \land \text{RC}(x, R).
\]

C. Proving Soundness of Learned Analysis Rules

While the learned analysis rules are correct by construction for the training examples, they may still be unsound when applied to unseen programs. We observe this, for example, in the leaves highlighted in red in Fig. 4c. Thus, \( \text{GPS} \) tries to confirm their soundness against the domain-specific knowledge base \( KB \). In the context of our running example—confirming soundness means proving that every variable \( x \) that is assigned type \( \text{RUD}(x) \) (resp. \( \text{SID}(x) \)) by the learned analysis rule \( \alpha \) is also certified \( \text{RUD}(x) \) (resp. \( \text{SID}(x) \)) by \( KB \).
We formalize the soundness proof as a Datalog query containment problem, and propose an algorithm based on bounded unrolling and k-induction to check it.

When applied to the candidate analysis of Fig. 4C the check results in the five counter-examples $CE_1, \ldots, CE_5$ with distribution type $UKD(CE_i)$ shown in Fig. 5. Each counter-example indicates the unsoundness of one path from the root of the decision tree to a classification node. These are abstract counter-examples in that they contain missing features and consequently do not define concrete ASTs. Thus, each of these abstract counter-examples is a set of feature valuations $\pi = \{f_1 \mapsto v_1, f_2 \mapsto v_2, \ldots, f_k \mapsto v_k\}$ that the current candidate analysis misclassifies, and feeding them back to the learner which results in additional abstract counter-examples in that they contain missing features.

With these new constraints from abstract counter-examples, the learner learns the new candidate analysis shown in Fig. 6. This new candidate analysis still has four unsound candidate rules, which results in additional abstract counter-examples when it is subjected to the soundness check. We repeat this back-and-forth between the rule learner and the soundness prover: after 11 iterations and after processing 27 counter-examples in all, $GPS$ learns the rules initially presented in Fig. 2b, all of which have been certified to be sound.

**D. Overall Architecture of the GPS System**

We summarize the architecture of $GPS$ in Fig. 1. The learner repeatedly applies DTL and SyGuS to learn candidate analyses that correctly classify training samples and are consistent with newly-added abstract counter-examples. Next, the prover checks the soundness of the learned analysis. Each subsequent counter-example is fed back to the learner which restarts the rule learning process on augmented dataset, until either all synthesized rules are sound or a time bound is exhausted.

**IV. LEARNING THE INFERENCE RULES**

We formally describe the analysis rule learner in Algorithm 1. The input consists of a set of labeled examples, $E$, and a set of pre-defined features, $F$. The output $T$ is a set of type-inference rules consistent with training examples. Each training example $(x, TYPE(x)) \in E$ consists of an AST node $x$ in a program and its distribution type $TYPE(x)$.

At the top level, the learner uses the standard decision tree learning (DTL) algorithm [30] as the baseline. However, if it finds that the current set $F$ of classification features is insufficient, it invokes a syntax-guided synthesis (SyGuS) algorithm to synthesize a new feature $f$ with strictly positive information gain to augment $F$. This allows the learner to combine the efficiency of techniques that learn decision trees with the expressiveness of syntax guided synthesis; similar ideas have been fruitfully used in other applications of program synthesis, see for example [31].

While the top-level classifier (e.g., Fig. 2b, 4b, 4c and 6) has a bounded number of decision points, the synthesized features (e.g., Fig. 3a) may be recursive. Furthermore, the newly synthesized features $f$ are induced as first-class citizens of $F$, and can subsequently be used at any level of the decision tree (see, for example Fig. 2b and 5). Next, we present the DTL and SyGuS subroutines respectively.

**A. The Decision Tree Learning Algorithm**

Recall that our pre-defined features (Fig. 4a) include properties of the AST node, such as $OP(x)$, and properties referring its left and right children, such as $OP(L) \land LC(x, L)$. The choice requires some care: having very few features will cause the learning algorithm to fail, while having too many features will increase the risk of overfitting. Our synergistic combination of DTL with SyGuS-based on-demand feature synthesis can be seen as a compromise between these extremes.

$DTL(E, F)$ is an entropy-guided greedy learner [30], where the entropy and conditional entropy of a set (defined below) are used to measure the diversity of its labels:

$$H(E) = - \sum_{i \in TYPE} \Pr(TYPE(x) = t) \log(\Pr(TYPE(x) = t))$$

$$H(E \mid f) = \sum_{i \in \text{Range}(f)} H(E \mid f(x) = i)$$

Algorithm 1 thus divides the set of training examples $E$ using the feature $f = f^*$ that minimizes the conditional entropy $H(E \mid f)$ (Lines 7–12), and recursively invokes the learning algorithm on each subset, $DTL(E \mid f(x) = i, F \setminus \{f^*\})$.

Observe that $H(E) = 0$ if $\Pr(TYPE(x) = t) = 100\%$, meaning purity or all examples $x \in E$ share the same type $TYPE(x) = t$. The difference between $H(E)$ and $H(E \mid f)$ is also referred to as the information gain. If the learner cannot
Algorithm 2 FeatureSyn(Ε).

Input: Examples, Ε = \{(x_1, TYPE(x_1)), \ldots, (x_n, TYPE(x_n))\}
Output: Feature f with positive information gain, or ⊥ to indicate failure

1. Let S be the meta-rules defined in Figure 2 i.e. the hypothesis space
2. for each relation schema r defined in S do
3. for each subset S of meta-rules corresponding to the schema do
4. for each choice p_in, q_in, and nested relational predicates do
5. Let f be the corresponding instantiation of the meta-rules in S
6. if h(Ε | f) ≤ h(Ε) then
7. return f
8. end if
9. end for
10. end for
11. end for
12. return ⊥

\[
R_f = \{ f(x) \leftarrow p_in(x), \]
\[ f(x) \leftarrow q_in(x,y), \]
\[ f(x) \leftarrow p_in(x,y) \land q_in(x,y), \]
\[ f(x) \leftarrow q_in(x,y) \land f(y), \]
\[ f(x) \leftarrow q_in(x,y) \land p_in(x) \land f(y) \}
\]

\[
R_g = \{ g(x,y) \leftarrow q_in(x,y), \]
\[ g(x,y) \leftarrow p_in(x) \land q_in(x,y), \]
\[ g(x,y) \leftarrow q_in(x,z) \land g(z,y), \]
\[ g(x,y) \leftarrow q_in(x,z) \land p_in(x) \land g(z,y) \}
\]

\[
R_h = \{ h(x) \leftarrow f(x) \land p_in(x) \land q_in(x,y), \]
\[ h(x) \leftarrow g(x,y) \land p_in(x) \land q_in(x,y), \]
\[ h(x) \leftarrow f(x) \land g(x,y) \land p_in(x) \land q_in(x,y) \}
\]

\[
p_{in}(x) ::= AND(x) \mid OR(x) \mid NOT(x) \mid XOR(x) \mid MUL(x) \mid LEAF(x) \]
\[ p_{in} \lor p_{in} \mid p_{in} \lor \neg p_{in} \]
\[
q_{in}(x,y) ::= LC(x,y) \mid RC(x,y) \mid DTL(x,y) \mid \neg q_{in} \mid q_{in}(x,y) \land q_{in}(x,y) \land q_{in}(x,y) \land q_{in}(x,y) \land q_{in}(x,y) \land q_{in}(x,y) \land \neg q_{in}(x,y) \]

Fig. 7. Syntax of the DSL for synthesizing new features.

find a feature with strictly positive information gain (Line 4), it will invoke the feature synthesis algorithm on Line 5.

B. The On-Demand Feature Synthesis Algorithm

We represent newly synthesized features as Datalog programs. Datalog is an increasingly popular medium to express static analyses [32–35], and its recursive nature enables the newly learned features to represent arbitrarily deep properties of AST nodes. A Datalog rule is a constraint of the form

\[
h(x) \leftarrow b_1(y_1) \land b_2(y_2) \land \cdots \land b_n(y_n),
\]

where h, b_1, \ldots, b_n are relations with pre-specified arities and schemas, and where x, y_1, \ldots, y_n are vectors of typed variables. Each rule can be interpreted as a logical implication: if b_1 \ldots b_n are true, then so is h. The semantics of a Datalog program is defined as the least fixed-point of rule application [36]; the solver starts with empty output relations, and repeatedly derives new output tuples until no new tuples can be derived.

Program synthesis commonly restricts the space of target concepts and biases the search to speed up computation and improve generalization. One form of bias has been to constrain the syntax: this has been formalized as the SyGuS problem [37] and as meta-rules in inductive logic programming [38, 39]. A meta-rule is construct of this form

\[
X_h(x) \leftarrow X_1(y_1) \land X_2(y_2) \land \cdots \land X_n(y_n)
\]

Here, X_1, X_2, \ldots, X_n are relation variables whose instantiation yields a concrete rule. Fig. 7 shows the meta-rules used in our work. For example, instantiating the meta-rule \( f(x) \leftarrow q_{in}(x,y) \land p_{in}(x) \land f(y) \) with \( q_{in}(x,y) = RC(x,y) \) and \( p_{in}(x) = XOR(x) \) yields \( f(x) \leftarrow RC(x,y) \land XOR(x) \land f(y) \).

There are three variations of the final target relation schema, \( f(x), g(x,y) \) and \( h(x) \), where x and y denote AST nodes.

We formalize the synthesis problem as that of choosing a relation \( R \in \{ f(x), g(x,y), h(x) \} \) and finding a subset \( P_D \) of its instantiated meta-rules from Fig. 7 such that the resulting Datalog program \( P_D \) has strictly positive information gain on the provided training examples \( \mathcal{E} \).

Algorithm 2 shows the procedure, which repeatedly instantiates the meta-rules from Fig. 7 and computes their information gain. It successfully terminates when it discovers a feature that can improve classification. Otherwise, it returns failure (upon timeout) and invokes DTL(Ε, F) to conservatively classify the decision tree node as being of type UKD.

Example IV.1. Given \( \mathcal{E} = \{ b_4, RUD, (n_1, UKD) \} \) shown in Fig. 2a, the synthesizer may alternatively learn the rules in Equations 3, 4 and 8:

\[
f(x) \leftarrow INRAND(x),
\]
\[ f(y) \leftarrow LC(y, x) \land f(x), \]
\[ f(y) \leftarrow RC(y, x) \land f(x), \]
\[ RUD(x) \leftarrow \neg RUD(x) \land LC(x, L) \land RC(x, R) \land RUD(L) \land f(R). \]

\[
g(x, z) \leftarrow \neg INRAND(x),
\]
\[ g(y, z) \leftarrow LC(y, x) \land g(x, z), \]
\[ g(y, z) \leftarrow RC(y, x) \land g(x, z), \]
\[ h(x) \leftarrow LC(x, L) \land RC(x, R) \land g(L, x_L) \land g(R, x_R) \land x_L = x_R, \]
\[ RUD(x) \leftarrow \neg RUD(x) \land RUD(L) \land LC(x, L) \land RC(x, R) \land \neg h(x). \]

Since the information gain of Rule 3 applying to \{ b_4, n_1 \} is zero, it gets discarded (Line 6 in Algorithm 2). In contrast, the information gains of Rules 4 and 5 are both positive. Rule 4 intuitively requires that both the left and right operands of x are of type RUD, and that they do not share any random inputs in computing \( \neg h(x) \). Rule 5 requires that the same secret key be used in the computation of both operands. While Rule 4 is sound when applied to arbitrary programs, Rule 5 is unsound. In the next section, we will present an algorithm that can check the soundness of these learned rules.

V. PROVING THE INFERENCE RULES

We wish to prove that a learned rule, denoted \( \alpha \), never reaches unsound conclusions when applied to any program, by showing that it can be deduced from a known-to-be-correct
knowledge base (KB). More specifically, we wish to confirm that every AST node $x$ marked as RUD (or SID) by $\alpha$ can be certified to be RUD (or SID) by $KB$. When both $\alpha$ and $KB$ are expressed in Datalog, the problem reduces to one of determining query containment, e.g., for every valuation of the input relations, $RUD_{\alpha} \subseteq RUD_{KB}$ (or $SID_{\alpha} \subseteq SID_{KB}$). We will now describe a semi-decision procedure to verify the soundness of the learned rules $\alpha$, which forms the second phase of the synthesis loop in GPS.

A. Representation of the Learned Rule ($\alpha$)

Let $\alpha$ be a set of Datalog rules, each of which has a head relation $\phi_\alpha$ and a body of the following form:

$$\phi_\alpha(x) \leftarrow \phi_1(x_1) \land \phi_2(x_2) \cdots \land \phi_n(x_n) \quad (6)$$

It means $\phi_\alpha$ holds only when all of $\phi_1, \ldots, \phi_n$ hold. Here, $\phi_\alpha$ may be a distribution type, e.g., $SID(x)$, or a recursive feature $g(x, y)$, e.g., representing that $x$ depends on $y$.

B. Representation of the Knowledge Base (KB)

Our $KB$ consists of two sets of proof rules, one for propositional logic and the other for distribution types.

Proof Rules for Propositional Logic. Fig. 8 shows the proof rules that represent axioms of propositional logic [40]; they can be used to reduce any valid (resp. invalid) Boolean formula to constant true (resp. false). Thus, they are useful in showing results such as $true \lor P$ and $false \land Q$ are secret-independent (SID), for arbitrary logical sentences $P$ and $Q$.

Consider the example rule $\alpha$ below, where $g_1$ and $g_2$ are synthesized features shown as dashed boxes in Fig. 9.

$$SID(x) \leftarrow OR(x) \land LC(x, L) \land RC(x, R) \land OR(L) \land OR(R) \land g_1(L, k_1) \land g_2(R, k_2) \land EQ(k_1, k_2)$$

$$g_1(L, k_1) \leftarrow INKEY(k_1) \land INRAND(r_1) \land LC(L, k_1) \land RC(L, r_1)$$

$$g_2(R, k_2) \leftarrow INKEY(k_2) \land LC(R, k_2)$$

Since $k_1 = k_2$, we transform $\alpha$ into an equivalent logic formula:

$$SID(x) \leftarrow EQ(x, (k_1 \land r_1) \lor (-k_1))$$

Rules $B1$, $B7$ and $Bf$ in Fig. 8 show that $(k_1 \lor r_1) \lor (-k_1)$ is always true. Thus, $x$ is always true. Since $x$ is a constant, we have $SID(x)$, meaning $x$ is secret-independent.

Such SID rules, learned by our method automatically, and yet overlooked by state-of-the-art, hand-crafted analyzers [11], [2], can significantly improve the accuracy of side-channel analysis on many programs.

Proof Rules for Distribution Types. Fig. 10 shows the proof rules that represent properties of the distribution types. They were collected from published papers [2], [16], [23] that focus on verifying masking countermeasures, which also provided the soundness proofs of these rules. For brevity, we omit the detailed explanation. Instead, we use Rule $D2.1$ as an example to illustrate the rationale behind these proof rules.

In Rule $D2.1$, the $dom(x, S)$ relation means that variable $x$ is masked by some input from the set $S$ of random inputs. For example, in $y = x_1 \oplus x_2$, where $x_1 = k \oplus r_1 \oplus r_2$ and $x_2 = b \oplus r_2$, we say that $x_2$ is masked by $r_2$, and $x_1$ is masked by both $r_1$ and $r_2$. However, since $r_2 \oplus r_2 = false$, $y$ is masked only by $r_1$. Thus, $dom(y, \{r_1\})$ holds, but $dom(y, \{r_2\})$ does not hold. In this sense, Rule $D2.4$ defines a masking set. For $y$, it is $S_y = (\{r_1, r_2\} \cup \{r_2\}) \setminus \{\{r_1, r_2\} \cap \{r_2\}\} = \{r_1\}$, which contains $r_1$ only. The masking set defined by $D2.4$ is useful in that, as long as the set is not empty, the corresponding variable is guaranteed to be of the RUD type.

C. Proving the Soundness of $\alpha$ Using $KB$

To prove that for every AST node $x$ marked as RUD$_{\alpha}(x)$ (resp. SID$_{\alpha}(x)$) by $\alpha$, it is also marked as RUD$_{KB}(x)$ (resp. SID$_{KB}(x)$) by $KB$, we show that the following relation $Ind(x)$ is empty for any valuation of the input relations:

$$Ind(x) \leftarrow \phi_\alpha(x) \land \neg \phi_{KB}(x) \quad (7)$$

where the relation $\phi$ may be instantiated to either RUD or SID. In theory, this amounts to proving query containment, which is undecidable for Datalog logic [41], [42], but there is a decidable Datalog fragment [41], [43], [44], and our metarules in Fig. 7 produce rules in this fragment.

First, we observe that every tuple $t = \phi(x)$ produced by a Datalog program is associated with one or more derivation trees. The heights of these derivation trees correspond to the depth of rule inlining at which the program discovers $t$. In particular, for each inlining depth $k \in \mathbb{N}$, each rule $\phi_h(x_h) \leftarrow \phi_1(x_1) \land \phi_2(x_2) \cdots \land \phi_n(x_n)$ is transformed into the rule:

$$\phi^{(k+1)}(x_h) \leftarrow \phi_1^{(k)}(x_1) \land \phi_2^{(k)}(x_2) \cdots \land \phi_n^{(k)}(x_n) \quad (8)$$

This rule is then used as a proof rule to prove that $\phi^{(k+1)}$ is true under certain conditions.
within propositional logic. For example, unrolling Proposition V.1.

\[ \text{Proposition V.1. If } \text{Ind}(k) (x) \text{ is an empty relation for each depth } k \in \mathbb{N}, \text{ then } \text{Ind}(x) \text{ is an empty relation.} \]

Observe that unrolling the rules of a Datalog program to any specific depth yields a formula which can be interpreted within propositional logic. For example, unrolling \( f(x) \) from Equation 3 at depths 1 and 2 gives us

\( f^{(1)}(x) = \text{INRAND}(x), \) and
\( f^{(2)}(y) = (\text{LC}(y, x) \land f^{1}(x)) \lor (\text{RC}(y, x) \land f^{1}(x)). \)

For any specific value of \( k \), we can therefore use an SMT solver to verify the emptiness of \( \text{Ind}(k) \).

\[ \text{For the induction step, in particular, we ask the SMT solver to check if } \text{Ind}(k) \text{ can be non-empty while the } i \text{ preceding relations } \text{Ind}(k-i), \ldots, \text{Ind}(k-1) \text{ are assumed to be empty.} \]

Here, \( \phi^{(k)}(x) \) is expressed recursively using \( \phi^{(k-1)}(x), \ldots, \phi^{(k-i)}(x) \)

and induction succeeds if there exists such a value for \( i \in \mathbb{N} \).

Let \( V^{(k)} \) be free variables introduced by unrolling the rules
at depth \( k \). We assert the non-emptiness of \( Ind^{(k)} \) below:

\[
\Phi^{(k)} = \bigvee_{x \in V^{(k)}} Ind^{(k)}(x).
\]

(10)

Thus, we formalize the induction step of the proof by constructing the following formula:

\[
\Psi^{(k)} = \neg \Phi^{(k-1)} \land \ldots \land \neg \Phi^{(k-1)} \land \Phi^{(k)}
\]

(11)

**Proposition V.2.** If for some \( i \in \mathbb{N} \), the relations \( Ind^{(1)}, \ldots, Ind^{(i)} \) are all empty (the base case), and the formula \( \Psi^{(k)} \) as defined above is unsatisfiable (the induction step), then \( Ind^{(k)} \) is empty for all \( k \in \mathbb{N} \).

Starting from \( i = 1 \), we use the SMT solver to check Proposition V.2 for increasingly larger \( i \) until a timeout is reached. If the SMT solver is ever successful in proving the proposition, it follows that the learned rule \( \alpha \) is sound.

**D. Generating Abstract Counter-Examples**

When the proof fails, however, we need to prevent the same rule from being learned again to guarantee progress. Let \( \pi = \{ f_1 = v_1, f_2 = v_2, \ldots, f_k = v_k \} \) be the feature valuation in the failing rule \( R_\pi \). We then construct the counter-example,

\[
CE_\pi = \{ (f \mapsto v) \mid (f, v) \in \pi \} \cup \{ f \mapsto -1 \mid f \in F \setminus \pi \}
\]

with label \( \text{UKD}(CE_\pi) \). Recall that \( F \) is the set of all features currently under consideration. Therefore, the feedback \( CE_\pi \) provided to DTL(\( \mathcal{E}, F \)) is an abstract counter-example, with all missing features \( f \in F \setminus \pi \) set to the unknown value \(-1\).

Consider the subsequent iteration of the decision tree learner, DTL(\( \mathcal{E} \cup \{ CE_\pi \}, F \)). Observe that whenever it is in a decision context which is also a prefix \( \pi_{\text{pre}} \) of the counter-example \( CE_\pi \), the information gain of each feature \( f \in \pi \) is strictly less than that encountered in the previous invocation. Therefore, at some level of the decision tree, it will either choose a different feature, or invoke the feature synthesis algorithm to grow \( F \).

By formalizing this argument, we say that:

**Proposition V.3.** Given a counter-example \( CE_\pi \) to a learned rule \( R_\pi \), the subsequent invocation of the learner DTL(\( \mathcal{E} \cup \{ CE_\pi \}, F \)) is guaranteed to no longer produce \( R_\pi \).

Before ending this section, we stress that the proof rules in \( KB \) should not be confused with analysis rules used in the learned analyzer, since they are way more computationally expensive. Consider Rule D1.4, whose Datalog encoding size for \( supp(x, S) \) would be \( |V| \times 2^{14N} \). For the benchmark named B19 in Table I it owns 1250 input variables and thereby causing the exponential explosion with \( 2^{1250} \). The learned rule \( \alpha \), in contrast, is much cheaper since it does not rely on these expensive set (union and intersection) operations.

**VI. EXPERIMENTS**

Our experiments were designed to answer the following research questions (RQs):

- **RQ1:** How effective is our learned analyzer in terms of the analysis speed and accuracy?

- **RQ2:** How effective is our \( \text{GPS} \) method for learning inference rules from training data?

- **RQ3:** How effective is our \( \text{GPS} \) method for proving the learned inference rules?

We implemented \( \text{GPS} \) in LLVM 3.6. \( \text{GPS} \) relies on LLVM to parse the C programs and construct the internal representation (IR). Then, it learns a static analyzer in two steps. The first step, which is SyGuS-guided decision tree learning, is implemented in 4,603 lines of C++ code. The second step, which proves the learned inference rules, is implemented using the Z3 [39] SMT solver. Furthermore, the learned analyzer for detecting power side channels in cryptographic software is implemented in LLVM as an optimization (opt) pass. We ran all experiments on a computer with 2.9 GHz Intel Core i5 CPU and 8 GB RAM.

**A. Benchmarks**

Our benchmarks are 568 programs with 2,691K lines of C code in total. They implement well-known cryptographic algorithms such as AES and SHA-3. Some of these programs are hardened by countermeasures, such as reordered MAC-Keccak computation [23], masked AES [16, 17], masked S-box calculation [49] and masked multiplication [50], to eliminate power side-channel leaks.

We partition the benchmarks into two sets: \( D_{\text{train}} \) for \( \text{GPS} \), and \( D_{\text{test}} \) for the learned analyzer. The training set \( D_{\text{train}} \) consists of 531 small programs gathered from various public sources, including byte-masked AES [51], random reduction of S-box [52], common shares [53], and leak examples [24]. Each benchmark is a pair, consisting of a program AST and its distribution type, i.e., the ground truth annotated by developers. The testing set \( D_{\text{test}} \) consists of 37 large programs, whose statistics (the number of lines of code and inputs labeled public, private, and random) are shown in Table I. Since these programs are large, it is no longer practical to manually annotate the ground truth; instead, we relies on the results of published tools: a (manually-crafted) static analyzer [1] for B1-B20 and a formal verification tool [2] for B21-B37.

---

**TABLE I**

**STATISTICS OF THE BENCHMARK PROGRAMS IN \( D_{\text{test}} \).**

| Name | Loc | \( L_{\text{train}} \) | \( L_{\text{test}} \) | \( L_{\text{train}} \) | Name | Loc | \( L_{\text{train}} \) | \( L_{\text{test}} \) | \( L_{\text{train}} \) |
|------|-----|----------------|----------------|----------------|------|-----|----------------|----------------|----------------|
| B1   | 11  | 0              | 2              | 2              | B2   | 12  | 0              | 2              | 2              |
| B3   | 12  | 0              | 1              | 1              | B4   | 16  | 0              | 3              | 1              |
| B5   | 25  | 1              | 4              | 4              | B6   | 32  | 1              | 1              | 3              |
| B7   | 11  | 1              | 7              | 7              | B8   | 82  | 1              | 1              | 7              |
| B9   | 104 | 1              | 7              | 7              | B10  | 904 | 1              | 16             | 16             |
| B11  | 1,130| 1            | 16              | 16             | B12  | 1,256| 0              | 25             | 75             |
| B13  | 2,804| 0              | 25              | 25             | B14  | 3,564| 0              | 1              | 175            |
| B15  | 3,810| 0              | 25              | 25             | B16  | 13,510| 0              | 25             | 257            |
| B17  | 18,858| 0            | 25              | 25             | B18  | 25,121| 0              | 25             | 975            |
| B19  | 22,225| 0            | 25              | 25             | B20  | 34,659| 0              | 16             | 232            |
| B21  | 24,599| 0            | 25              | 25             | B22  | 30,226| 0              | 16             | 232            |
| B23  | 25,024| 0            | 25              | 25             | B24  | 25   | 0              | 2              | 2              |
| B25  | 27   | 1              | 2              | 2              | B26  | 32   | 0              | 2              | 2              |
| B27  | 40   | 0              | 2              | 2              | B28  | 49   | 0              | 2              | 4              |
| B29  | 80   | 2              | 4              | 4              | B30  | 66   | 0              | 4              | 4              |
| B31  | 86   | 0              | 7              | 7              | B32  | 268  | 288            | 288            | 288            |
| B33  | 256  | 288            | 288            | 288            | B34  | 426k | 288            | 288            | 288            |
| B35  | 424k | 288            | 288            | 288            | B36  | 426k | 288            | 288            | 288            |

- **RQ2:** How effective is our \( \text{GPS} \) method for learning inference rules from training data?

- **RQ3:** How effective is our \( \text{GPS} \) method for proving the learned inference rules?
### B. Performance and Accuracy of the Learned Analyzer

To demonstrate the advantage of our learned analyzer (answer RQ1), we compared our learned analyzer with the two existing tools [1], [2] on the programs in $D_{test}$. Only our analyzer can handle all of the 37 programs. Therefore, we compared the results of our analyzer with the tool from [1] on B1-B20, and with the tool from [2] on B21-B37. The results are shown in Table II and Table III respectively.

In both tables, Columns 1-2 show the benchmark name and the number of AST nodes. Columns 3-6 show the existing tool’s analysis time and result, including a breakdown in three types. Similarly, Columns 7-10 show our learned analyzer’s time and result. Note that in [1], the UKD/SID/RUD numbers were the number of variables of the LLVM IR, and thus larger than the number of variables in the original programs. To be consistent, we compared with their results in the same manner in Table II.

The results in Table II and Table III show that our learned analyzer is much faster, especially on larger programs such as B20 (3.6 seconds versus 16 minutes). The reason why our analyzer is faster is because the manually-crafted analyses [1], [2] rely on evaluating set-relations (e.g., difference and intersection of sets of random variables), whereas our DSL syntax is designed without set operations to infer the same types, thus leading to faster analyses. Although in general the set operation-based algorithm is more accurate, it has excessive computational overhead. Moreover, it does not always improve precision in practice. Furthermore, the method in [2] uses an SMT solver-based model counting technique to infer leak-free variables, which is significantly more expensive than type inference.

As shown in Table II and Table III by learning inference rules from data, we can achieve almost the same accuracy as manually-crafted analysis [1], [2] while avoiding the huge overhead. Given the same definitions of distribution types (UKD, SID, and RUD), both our learned rules and manually-crafted analysis rules [1], [2] can infer the non-leaky patterns, thus recognizing the variable types correctly under most benchmark, in Table II and Table III except for B4-B6 and B30, where set operations are required to prove the leak-freedom of some variables. Recall that losing accuracy here indicates that our learned rules infer the types more conservatively, without losing soundness. Nevertheless, our analyzer also increased accuracy in some other cases (e.g., B2), due to its deeper constant propagation (which led to the proof of more SID variables) while the existing tool [1] failed to do so, and conservatively marked them as UKD variables.

### C. Effectiveness of Rule Induction and Soundness Verification

To answer RQ2 and RQ3, we collected statistics while applying GPS to the 531 small programs in $D_{test}$, as shown in Table IV. In total, GPS took 30 iterations to complete the entire learning process. Column 1 shows the iteration number and Column 2 shows the time taken by the learner and the prover together. Columns 3-6 show the number of inference rules learned during each iteration, together with their types (UKD, SID, and RUD). Similarly, Columns 7-10 show the number of verified inference rules and their types.

The next two columns show the following statistics: (1) the size of the learned decision tree (# Treelearn) in terms of the number of decision nodes; (2) the number of counter-examples (CEX) added by the prover (# ASTCEx), which are added to the 531 original training programs before the next iteration starts. The last column shows the number of features generated by SyGuS; these features are also added to the original feature set and then used by the learner during the next iteration.

Results in Table IV demonstrate the efficiency of both the learner and the prover. Within the learner, the number of rules produced in each iteration remains modest (8 on average), indicating it has successfully avoided overfitting. This is because the SyGuS solver is biased toward producing small features which, by Occam’s razor, are likely to generalize well. Furthermore, any learned analysis rules have to pass the soundness check, and this provides additional assurance against overfitting to the training data. The prover either quickly verifies a rule, or quickly drops it after adding a counter-example to prevent it from being learned again. In early iterations, about half of all learned rules can be proved, but as more counter-examples are added, the quality of the
TABLE IV
DECISION TREE LEARNING WITH FEATURE SYNTHESIS (DIFFERENT ITERATIONS WITH #AST = 531).

| Iteration | Time (s) | # Rules Learned | % Rules Verified | # Rules Verified | % AST/EX | # Feature/learning | # Feature/verifying |
|-----------|----------|----------------|------------------|-----------------|-----------|-------------------|--------------------|
| 1         | 1.316    | 10             | 50               | 4               | 5         | 23                | 4                  |
| 2         | 0.778    | 8              | 2                | 5               | 2         | 1                 | 1                  |
| 3         | 0.517    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 4         | 0.517    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 5         | 0.517    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 6         | 0.517    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 7         | 0.517    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 8         | 0.517    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 9         | 0.517    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 10        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 11        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 12        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 13        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 14        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 15        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 16        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 17        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 18        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 19        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 20        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 21        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 22        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 23        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 24        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 25        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 26        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 27        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 28        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 29        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |
| 30        | 0.524    | 8              | 2                | 4               | 2         | 2                 | 1                  |

TOTAL: 186893 237 63 60 114 167 54 56 1071 1833 622

learned rules improves, and thus the percentage of proved rules also increases.

D. Threats to Validity

Our experimental evaluation focused on cryptographic software, which is structurally simple and, unlike general-purpose software, does not exercise complicated language constructs. It is an interesting direction of future work to extend our techniques to these more general classes of software code.

A notable limitation in our work is the assumption of the knowledge base (KB). While KB is readily available for our application (side-channel analysis), for other applications, it might be non-trivial to construct. Furthermore, an incorrect KB might compromise the soundness of the learned rules, although in this work, we have carefully mitigated this threat by curating the proof rules from previous papers [2], [16], [24] that have themselves formally verified the validity of these proof rules.

VII. RELATED WORK

Generating Analyzers from Examples. While there are prior works on learning static analyzers [5], [54], they do not guarantee soundness. For example, the analyzer learned by Bielik et al. [5] is sound with respect to programs in the training set, not all programs written in the same programming language (JavaScript). They also need to manually modify the training programs to generate counter-examples, while our method generates counter-examples automatically.

Formal Specifications. There are also works on synthesizing static analyzers from formal specifications, e.g., proof rules or second-order logic formulas [29], [55], [56] as opposed to training data. However, they restrict the logic used to write the specification, and as a result, may not be expressive enough to synthesize practical analyzers. Users are also expected to write correct specifications, which is a non-trivial task. In addition, they cannot exploit the information provided by data.

Learning-based Techniques. There are several prior techniques using machine learning to conduct static program analyses [57]–[60]. Such techniques focus on finding a suitable program-to-feature embedding. However, they require the user to perform feature engineering, which is known to be laborious. Some of these techniques [58], [61]–[63] do not take advantage of new features that may be learned from data; instead, they build classifiers based solely on existing features. In contrast, our method not only learn new analysis rules from data, but also use SyGuS to synthesize new features automatically.

Optimizing an Analyzer. It is possible to optimize an existing static analyzer [57], [64]–[68], which can be achieved by adjusting the level of abstraction [64], [65], [69]. Learn heuristics and parameters [66], make soundness-accuracy trade-offs [67], or select sound transformers [68]. However, such techniques fundamentally differ from our method because they assume the analyzer is already given, and focus on optimizing its performance, whereas we focus on synthesizing a new analyzer.

Syntax-Guided Synthesis. Since we automatically generate new features, our method is related to the large and growing body of work on SyGuS. While SyGuS has been used in various applications [70]–[80], none of them aims to synthesize a provably sound static analyzer from data. While some of these existing techniques can synthesize Datalog rules [39], [81], [82], the focus has been on efficiency, e.g., pruning the search space based on syntactic structures, instead of guaranteeing the soundness of the analyzer.

Power Side-Channel Analysis. In this work, we use power side-channel analysis as the application to evaluate our method. In this sense, it is related to the body of work on side-channel...
leak detection \cite{2-4, 83-85} as well as mitigation \cite{1, 24, 28, 86-88}. While static analysis engines used in these existing works are all hand-crafted by domain experts, our method aims to synthesize the static analysis from data automatically.

VIII. CONCLUSIONS

We have presented a data-driven method for learning a provably sound static analyzer to detect power side channels in cryptographic software. It relies on SyGuS to generate features and DTL to generate analysis rules based on the synthesized features. It verifies the soundness of these learned analysis rules by solving a query containment checking problem using an SMT solver. We have evaluated our method on C programs that implement well-known cryptographic protocols and algorithms. Our experimental results show that the learning algorithm is efficient and the learned analyzer can achieve the same empirical accuracy as state-of-the-art analysis tools while being several orders-of-magnitudes faster.

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