Optical detection of paramagnetic defects in diamond using off-resonance excitation of NV centers

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In this work we use fluorescence from nitrogen-vacancy defects in diamond to detect and explore other paramagnetic defects in the diamond, such as P1 defects, which are commonly undetectable through optical detection of magnetic resonance in standard conditions. Our method does not require overlap between the defects’ resonances and therefore is applicable in a wide region of magnetic fields and frequencies, as verified by excellent fit to theoretical predictions. We propose a depolarization scheme of P1 defects to account for the observed data. To verify our results, we perform cavity-based detection of magnetic resonance and find a good agreement between the measured optically induced polarization and the value obtained theoretically from rate equations. The findings in this work may open the way to detection of paramagnetic defects outside of the diamond through the photoluminescence of nitrogen-vacancy defects, which might be useful for imaging in biology.

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I. INTRODUCTION

The nitrogen-vacancy (NV) defect in diamond consists of a substitutional nitrogen atom (N) combined with a neighbor vacancy (V) \([1]\). In its negatively-charged state the NV\(^−\) defect has a spin triplet ground state \([2]\) having relatively long coherence time \([3]\). The NV\(^−\) spin state can be polarized via the process of optically-induced spin polarization (OISP) \([4, 5]\) and can be measured using the technique of optical detection of magnetic resonance (ODMR) \([6–8]\). These properties facilitate a variety of applications including magnetometry \([9]\) and sensing \([10–12]\).

ODMR of diamond samples having relatively low density of spin defects is commonly described using a single-spin model, in which dipolar coupling between different spins is disregarded. However, this approach becomes invalid when the spin density is sufficiently high. In general, the strength of the dipolar coupling can be characterized by the magnetic susceptibility \(\chi\). At the Larmor frequency, the magnetic susceptibility of a spin \(1/2\) ensemble having a number density \(n_S\) is given by \(\chi = i (n_S/n_{S0}) P_{30}\), where \(P_{30}\) is the spin polarization in steady state and the density \(n_{S0}\) is given by \(n_{S0} = 4T_2^{-1}h_e^2\mu_0\), where \(T_2^{-1}\) is the transverse spin relaxation rate, \(\gamma_e = 2\pi \times 28.03\ \text{GHz T}^{-1}\) is the electron spin gyromagnetic ratio and \(\mu_0\) is the permeability of free space \([13, 14]\). The transverse spin relaxation rate of our sample \(T_2^{-1} \approx 0.1\ \text{MHz}\) yields the value of \(n_{S0} \approx 10^{17}\ \text{cm}^{-3}\), which is about 3 times smaller than the number density of NV\(^−\) defects in our sample. Thus, when the polarization \(|P_{30}|\) becomes of order unity by applying OISP \([4, 5]\), \(\chi\) cannot be treated as a small parameter, and dipolar coupling cannot be disregarded.

In the current study we investigate diamond samples having relatively high density of both NV\(^−\) and nitrogen 14 substitution (P1) defects. The spin density of our samples is not sufficiently high to allow access to the region where macroscopic magnetic ordering occurs \([21]\), however it is sufficiently high to make \(\chi \gtrsim 1\), i.e. to make effects originating from dipolar coupling detectable. To further enhance such effects, the sample is cooled down to a cryogenic temperature of 3.6 K in order to decrease the rate of thermal polarization, which in turn makes OISP more efficient.

While only transitions between spin states with magnetic quantum numbers \(m_s = \pm 1\) and \(m_s = 0\) of NV\(^−\) are commonly visible in the ODMR spectrum of diamond samples, our ODMR measurements reveal magnetic resonances of P1 defects \([21–23]\), as well as resonances due to carbon 13 (C13) atoms, NV\(^−\) +1 \(\rightarrow\) –1 transitions and a resonance of unknown origin around 2 GHz found at magnetic fields near the NV\(^−\) ground-state level anticooperating (GSLAC). The observation of nuclear and electronic spin transitions in P1 defects can be attributed to driving-induced depolarization and a cross-relaxation process \([24–26]\) between the NV\(^−\) defects and the target spins under driving. These processes might be of interest in the context of nuclear spins ensembles hyperpolarization \([27–29]\), with NV\(^−\) defects providing an optical path for readout and control.

To further explore dipolar coupling in our samples, the method of cavity-based detection of magnetic resonance (CDMR) is employed \([30]\). As discussed below, the results of the CDMR measurements provide further insight into the underlying mechanism responsible for dipolar coupling in our samples. In particular, these results clearly rule out the possibility that heating plays an important role in this mechanism.

In addition, the CDMR measurements allow studying the process of OISP in general, and the prospects of employing OISP for the generation of spin population inversion, which, in-turn, may allow the realization of a diamond-based maser. A maser is constructed by coupling an ensemble of emitters to a microwave cavity and by applying external pumping for inducing population inversion. A maser has a variety of applications, including amplification of microwave signals, high-precision tim-
ing, optical to microwave conversion, magnetometry and spectroscopy. The process of OISP can be used for inducing population inversion in diamond when the externally applied magnetic field is tuned to the region above the NV$^-$ GSLAC point. This together with the relatively long coherence time $T_2$ and long energy relaxation time $T_1$, makes the NV$^-$ defects in diamond useful for the construction of a maser, as has been recently proposed $[31]$ and demonstrated experimentally $[33]$. In this work, we generate population inversion, though we do not reach the masing threshold due to anomalous saturation of the polarization of NV$^-$ spins, which is consistent with previous observations $[26, 34]$.

II. EXPERIMENTAL SETUP

The experimental setup is schematically depicted in Fig. 1. Defects in a [110] type Ib diamond are created using 2.8 MeV electron irradiation with a dose of approximately $8 \times 10^{18}$ e/cm$^2$, followed by annealing at 900°C for 2 hours and acid cleaning, resulting in the formation of NV$^-$ defects with density of $n_S \simeq 3.25 \times 10^{17}$ cm$^{-3}$ $[44]$.

Two multimode optical fibers are glued to the irradiated diamond using optical adhesive. The one labeled as F1 in Fig. 1(a) is used for delivering laser light having wavelength of 532 nm to the sample, and the one labeled as F2 transmits the photoluminescence (PL) emitted from the sample. The diamond is attached to a sapphire wafer supporting a spiral shaped superconducting microwave cavity (resonator $[45, 46]$). The spiral is made of 180 nm thick niobium, has 7-turns, inner diameter of 0.7 mm and width and spacing of 40 μm. In the first part of this work, the delivered light intensity is relatively high and consequently the resonator is heated above its critical temperature and is effectively disabled, while in the second part, the light intensity is reduced and the resonator may be used as a superconducting cavity. A three-loop antenna (LA) is placed in the vicinity of the diamond. An amplitude modulated signal at frequency $f_p$ is injected into the LA, and the modulation signal serves as a reference for a lock-in amplifier connected to a photodiode collecting the filtered PL (605 nm). A superconducting solenoid magnet is used for applying magnetic field $B$. The setup is cooled down to a base temperature of 3.6 K to enhance hyperpolarization of non-NV impurities $[47]$.

The spatial orientation of the sample with respect to the externally applied magnetic field is characterized by a unit vector $\hat{n}_{MA} = (\sin \theta_{MA} \cos \varphi_{MA}, \sin \theta_{MA} \sin \varphi_{MA}, \cos \theta_{MA})$. In this work, we use several orientations to confirm our theoretical predictions. The angles for the data presented in Fig. 2 and Fig. 3 are $\theta_{MA} = -4^\circ$ and $\varphi_{MA} = 95^\circ$, in Fig. 4 $\theta_{MA} = -12.3^\circ$ and $\varphi_{MA} = 95^\circ$, in Fig. 5 $\theta_{MA} = -9.5^\circ$ and $\varphi_{MA} = 94.5^\circ$, whereas the angles used for the CDMR measurements in Fig. 6 are $\theta_{MA} = -1.85^\circ$ and $\varphi_{MA} = 97^\circ$.

III. NV$^-$

The NV$^-$ ground state spin triplet Hamiltonian is given by $[36, 37]$

$$\frac{\mathcal{H}_{NV^-}}{\hbar} = DS_1^2 - \gamma_e B \cdot S_1 + \frac{E_{NV^-} (S_{1,+}^2 + S_{1,-}^2)}{2},$$

where $D$ is the zero field splitting induced by spin-spin interaction, $S_1 = (S_{1,x}, S_{1,y}, S_{1,z})$ is a vector electronic spin operator, $B$ is an externally applied magnetic field, $E_{NV^-}$ is the strain-induced splitting, the raising $S_{1,+}$ and lowering $S_{1,-}$ operators are defined by $S_{1,\pm} = S_{1,x} \pm i S_{1,y}$ and the NV$^-$ axis is parallel to the z axis.

The color-coded plot shown in Fig. 2(a) represents the normalized lock-in signal as a function of the frequency of the applied microwave signal $f_p$ and the externally applied stationary magnetic field $B$. In a single crystal diamond the NV defects have four different possible orientations. The two frequencies per orientation corresponding to the transitions between the spin state with magnetic quantum number 0 and the spin state with magnetic quantum number ±1 are calculated by diagonalizing the Hamiltonian $[11]$ [see Fig. 6(b)], and are shown in by the black dashed lines in Fig. 2(b). A fitting procedure allows
FIG. 2: ODMR. (a) Color coded plot of the normalized ODMR signal as a function of frequency $f_p$ and magnetic field $B$. (b) The overlaid black (green) dashed lines represent NV$^-$ ground state $\pm 1$ to 0 ($+1$ to $-1$) transitions and are calculated by numerically diagonalizing the NV$^-$ ground state spin triplet Hamiltonian $H_{NV^-}$. The red dashed lines are obtained by adding the hyperfine interaction term $V_{NV^-C}$ (2) to the Hamiltonian $H_{NV^-}$. The white dotted lines represent P1 electronic-like transitions, calculated using the Hamiltonian $H_{P1}$. Higher order hyperbolas corresponding to multi-photon resonances are also observed and are discussed in [35]. The following values are assumed in the calculations: $D = 2\pi \times 2.88$ GHz, $E_{NV^-} = 2\pi \times 10$ MHz [36, 37], $A_{C,\parallel} = 2\pi \times 199.7$ MHz, $A_{C,\perp} = 2\pi \times 120.3$ MHz [38–42], $Q_{p1} = -2\pi \times 3.97$ MHz, $A_{P1,\parallel} = 2\pi \times 114$ MHz and $A_{P1,\perp} = 2\pi \times 81.3$ MHz [43]. (c) ODMR in the high frequency regime showing the ground state level anticrossing (GSLAC). (d) See (b). (e) Resonance lines of unknown origin. Cyan dotted line represents fit to Eq. (4).

determining the sample orientation (characterized by the angles $\theta_{MA}$ and $\varphi_{MA}$) with respect to the externally applied magnetic field. Additional resonance frequency per NV$^-$ orientation is seen in the ODMR spectra and is marked by green dashed lines in Fig. 2(b,d). It corresponds to the transition between states with magnetic quantum numbers $+1$ and $-1$. When the NV$^-$ vector and the magnetic field are not strictly parallel, or near the GSLAC, these states acquire a non-negligible component of 0 spin state, and hence the transition between them becomes measurable with ODMR [1]. At some combinations of the magnetic field orientation and magnitude, these transitions might be useful for magnetometry with higher responsivity than the one obtained with the more commonly used $0 \rightarrow \pm 1$ transitions, due to the two-times larger pre-factor of $2\gamma_e$. In order to verify our results, we repeat the same procedure using different orientation of the sample. For both cases excellent fit is obtained (see Figs. 2 and 4).

IV. CARBON 13

The hyperfine interaction between an NV$^-$ defect and the nearest-neighbor carbon-13 atom has been studied in [38–42]. To account for this interaction, a coupling term $V_{NV^-C}$ given by [43, 48]

$$\frac{V_{NV^-C}}{\hbar} = S_1 R_{C}^{-1} A_C R_C I_{1/2},$$

(2)

is added to the Hamiltonian $H_{NV^-}$, where $I_{1/2}$ is a vector nuclear spin 1/2 operator, the matrix $A_C$ is given by $A_C = \text{diag}(A_{C,\perp}, A_{C,\perp}, A_{C,\parallel})$, where $A_{C,\parallel}$ and $A_{C,\perp}$ are respectively the longitudinal and transverse hyperfine coupling parameters. The matrix $R_C$ is a rotation matrix satisfying $R_C \hat{n}_C = \hat{z}$, where $\hat{n}_C$ is a unit vector parallel to the vacancy-carbon axis and $\hat{z}$ is a unit vector in the $z$ direction. The overlaid red dashed lines in Figs. 2(b) and 4(b) are calculated by numerically diagonalizing the NV$^-$ Hamiltonian $H_{NV^-}$ with the added hyperfine coupling term (2).
in Fig. 5(b), nuclear-like transitions corresponding to the numbered in Fig. 3(a). Electronic-like transitions corresponding to the pairs (6, 1), (5, 2) and (4, 3) are seen in Fig. 5(b), nuclear-like transitions corresponding to the pairs (6, 5), (5, 4), (3, 2) and (2, 1) in Fig. 5(c) and two mixed transitions corresponding to the pairs (6, 3) and (5, 3) in Fig. 5(d). To our knowledge, this is the first reported observation of P1 nuclear-like transitions through PL of NV defects in diamond.

The visibility of P1 nuclear and electronic spin transitions in the ODMR data could be explained by resonant microwave heating, however this hypothesis contradicts CDMR measurements, as will be discussed below in Sec. VII. Alternatively, we attribute the visibility of P1 resonances in the ODMR data to a reverse-hyperpolarization process. In general, large imbalance in spin polarization between P1 and NV$^-$ defects can be induced by applying OISP, which significantly enhances spin polarization of NV$^-$ defects. In the absence of any coupling between P1 and NV$^-$ defects, the spin polarization of P1 defects is expected to be unaffected by the optical pumping, and remains at the value corresponding to thermal equilibrium. However, finite coupling is expected to give rise to optically-induced enhancement in the P1 spin polarization. Such enhancement is observed in our CDMR measurements and is discussed in Sec. VII below. On the other hand, the opposite effect of P1 depolarization can be induced by applying radiofrequency (RF) signal at a frequency close to a P1 transition resonance. Such P1 driving-induced depolarization, in-turn, is expected to give rise to NV$^-$ depolarization, due to the coupling between the two ensembles. The observed change in the ODMR signal is attributed according to this mechanism to such an NV$^-$ depolarization. Rate equations for this reverse-hyperpolarization process are given in Appendix A.

\section{VII. UNIDENTIFIED RESONANCE}

While we have been able to identify most resonance lines in the ODMR plot, an unidentified pronounced feature appears when better alignment is achieved [see Fig. 2(c)]. The observation that this feature is symmetrical around $\sim 102$ mT (GSLAC of NV$^-$) suggests that it originates from a coupling between the NV$^-$ defects having axis nearly parallel to B and a resonance having a magnetic field independent frequency. However, we could not find any evidence for such resonance in our measurements (both optical and microwave reflection). Interestingly, the frequency $f_I$ of this resonance line may be fitted by using the following relation [see cyan dashed line in Fig. 2(c)]

$$f_I = F_s - \frac{F_{NV^-}}{3},$$

where $F_s = 2.169$ GHz and $F_{NV^-}$ is the B-dependent resonance frequency of the $-1 \to 0$ transition of the NV$^-$ defects having axis nearly parallel to B [see black dashed lines in Fig. 2(b)]. In a different cooling cycle and alignment, we find Eq. (4) to fit the data well with $F_s = 2.172$ GHz.
FIG. 4: Rotated configuration. (a) ODMR data obtained by rotating the sample by about 10° with respect to the configuration used for generating the data shown in Fig. 2(a). (b) Theoretical calculation of resonance lines due to NV$^-\pm1\rightarrow0$ transitions (black), NV$^-+1\rightarrow-1$ transitions (green), carbon 13 (red) and P1 (white) defects. All lines were obtained by modifying only the diamond rotation angles.

FIG. 5: Normalized ODMR in the region of relatively small magnetic field. The overlaid white dotted lines represent (b) electronic-like, (c) nuclear-like and (d) mixed transitions in P1.

VII. CDMR MEASUREMENTS

In this section, we reduce the injected light intensity to avoid heating of the superconducting spiral resonator located below our diamond sample, so the resonator regains its superconductive properties and may be used as a cavity. We employ the method of CDMR as discussed in [30]. We apply reflection measurements using a network analyzer to extract the reflection coefficient $S_{11}$, which is given by [55]

$$S_{11} = \frac{i(\omega_p - \omega_0) - (\gamma_2 - \gamma_1)}{i(\omega_p - \omega_0) - (\gamma_2 + \gamma_1)},$$

where $\omega_0 \simeq 2\pi \times 1.464$ GHz is the cavity angular resonance frequency, $\omega_p$ is the angular frequency of the injected signal and $\gamma_1$ and $\gamma_2$ are coupling coefficients associated with the antenna-resonator and the resonator-reservoir (dissipation) couplings, respectively. Note that the cavity resonance frequency is set to the crossing point between NV$^- -1\rightarrow0$ and P1 electronic-like transitions. We fit our data and find $\gamma_1 = 1.15$ MHz and
\( \gamma_2 = 0.62 \text{ MHz (laser off)}, \) leading to a \( Q \)-factor of \( \sim 2500 \), and by assuming \( \gamma_1 \) is independent of laser power, we find \( \gamma_2 \) for various laser powers. Note that \( \gamma_1 > \gamma_2 \), i.e. the resonator is over-coupled (away from spin resonances). Figure 3(a) shows typical CDMR data with six resonances - five corresponding to P1 transitions and one to the NV \( ^{-1} \to 0 \) transition, whereas Fig. 3(b) is for magnetic field above the GSLAC, where the ground state of the NV\(-1\) triplet is the state having \( m_0 = -1 \) and the transition \( 0 \to -1 \) is seen. In the first case, we expect the coupling between the NV\(-1\) defects and the superconducting resonator to increase \( \gamma_2 \) due to increased losses. The opposite behavior is expected in the second case, since the state \( m_0 = 0 \), which is optically populated via OISP, is no longer the ground state of the system, and consequently some population inversion is expected, resulting in a decrease in \( \gamma_2 \). These phenomena are observed here and are shown in Figs. 3(c)-(d) for various laser intensities \( I_L \). For both cases, the process of optically-induced change in \( \gamma_2 \) exhibits a saturation for \( I_L \sim 10 - 15 \text{ mW mm}^{-2} \), which is similar to the anomalous saturation reported in 29, 34.

In an attempt to increase the loaded \( Q \)-factor, we move the antenna further away from the diamond-resonator sample. The reduced coupling to the antenna makes the resonator under-coupled (\( \gamma_1 < \gamma_2 \)) with \( \gamma_1 = 0.27 \text{ MHz} \). We repeat the same measurements and similar results are obtained.

The expected change in normalized cavity damping, which is denoted by \( \vartheta = \frac{\gamma_0}{\gamma_2} \), where \( \gamma_0 \) is the spin-induced change in the cavity damping rate, can be estimated using Eqs. (4) and (8) of Ref. [30]

\[
\vartheta = \frac{\kappa}{1 + \Delta^2 T_2^2} \frac{1 + \frac{T_{10}^{-1}}{T_{1T}^{-1}} \frac{P_{SO}(I_L)}{P_{ST}}}{1 + \frac{T_{10}^{-1}}{T_{1T}^{-1}}}.
\]

where \( \kappa \) is the cooperativity parameter characterizing the coupling between the spins and the cavity mode, \( \Delta \) is the frequency detuning between the cavity mode frequency and the spin’s transition frequency and \( T_{10}^{-1} (T_{1T}^{-1}) \) is the rate of OISP (thermal relaxation). In steady state and when \( T_{1T}^{-1} \gg T_{10}^{-1} \) (i.e. when OISP is negligibly small) the coefficient \( P_{ST} \) is the value of spin polarization \( P_z \) in thermal equilibrium. In the opposite limit of \( T_{10}^{-1} \gg T_{1T}^{-1} \) (i.e. when thermal relaxation is negligibly small) the coefficient \( P_{SO} \) is the value of \( P_z \) in steady state. The rate \( T_{10}^{-1} \) of OISP is expressed as \( T_{10}^{-1} = C_0 \gamma_0 \), where \( C_0 \) is a dimensionless parameter characterizing the absorption efficiency and where \( \gamma_0 = I_L \sigma \lambda_L / h \) is the rate of optical absorption, \( I_L \) is the laser intensity, \( \sigma = 3 \times 10^{-17} \text{ cm}^2 \) is the optical cross section, \( h \) is the Planck’s constant and \( c \) is the speed of light in vacuum. Note that Eq. (6) is obtained by assuming that all contributing spins share the same coupling to the cavity mode and to the laser light and that nonlinearity in the response can be disregarded.

The spin polarization \( P_z \) as a function of OISP rate \( T_{10}^{-1} \) can be extracted from the data shown in Fig. 3, using Eq. (6). Results of the extraction procedure are presented in Fig. 3(e)-(f) using blue pluses (red crosses) markers for NV\(-1\) (P1) for magnetic fields below [Fig. 3(e)] and above [Fig. 3(f)] the NV\(-1\) GSLAC. It can be seen from Fig. 3(e) that when the NV\(-1\) and P1 resonances coincide, polarization of both defects is of the same order of magnitude and OISP is \( \sim 1.6 \) times larger when compared to thermal polarization alone (laser off). The rate equations derived in appendix A are used to calculate the expected dependency of \( P_z \) on \( T_{10}^{-1} \). Solid lines in Fig. 3(e)-(f) are generated by solving Eqs. (A1) and (A2) (the parameters used for the fit are given in the caption of Fig. 3(e). The comparison between data and theory yields a good agreement.

In order to gain a further insight, we revisit CDMR data acquired with a different, yet similar, setup as described in 29, 34, where NV\(-1\) and P1 resonances do not coincide near the cavity frequency. Same analysis as described above is performed and OISP is found to be about 5 times larger for NV\(-1\) when compared to thermal polarization alone, but only 1.15 larger for P1 defects. These results suggest that the relative ineffectiveness of OISP that is revealed by Fig. 3(e) originates from the proximity between the frequencies of NV\(-1\) and electronic-like P1 transitions.

As was discussed above, when the externally applied magnetic field exceeds the value of \( \sim 102 \text{ mT} \) (i.e. above the NV\(-1\) GSLAC) the process of OISP is expected to increase (rather than decrease) the polarization \( P_z \). The plot in Fig. 3(f) demonstrates this behavior, and shows that this process gives rise to population inversion (i.e. a change in the sign of \( P_z \)). The largest measured value of \( |P_z| \) is about 15 times larger than the value corresponding to thermal equilibrium. This enhancement factor is significantly larger compared to the case where \( B < 102 \text{ mT} \) (see Fig. 3(e)]. However, it is not sufficiently large to allow reaching the threshold of masng. The threshold inaccessibility occurs due to the above-discussed anomalous saturation in the dependency of polarization upon laser power.

Note that the power of microwave driving used in the CDMR measurements is about 8 orders of magnitude lower than the power used in the ODMR measurements. This fact together with the significant hyperpolarization observed in the CDMR measurements excludes resonant microwave heating effects as being responsible for the visibility of P1 transitions in the ODMR data presented above.

**VIII. CONCLUSIONS**

Our results demonstrate that the P1 defects in diamond and the NV\(-1\) to \( +1 \) transition can be optically probed. In addition to electronic-like transitions in P1, we report here for the first time on an optical detection of both nuclear-like and mixed transitions. We show that these transitions are visible in a
FIG. 6: Cavity mode reflectivity showing (a) five P1 resonances and one NV$^-$ resonance and (b) one NV$^-$ resonance in the over-coupled resonator case. Fit to theory is shown using black dashed lines for NV$^- 0 \rightarrow -1$ transition [see Eq. (1)] and white dotted lines for P1 defects [see Eq. (3)]. (c)-(d) Change in normalized $\gamma_2$ with respect to the magnetic field for various laser powers (legends inside figures indicate values of laser intensity $I_L$ in units of mW mm$^{-2}$). Resonances due to P1 defects are marked by black arrows, while resonance due to NV$^- 0 \rightarrow -1$ transition is marked by a red circle. (e)-(f) Polarization $P_z$ as a function of OISP rate $T_{1O}^{-1}$. Markers (blue pluses for NV$^-$, red crosses for P1) denote data extracted from (c)-(d), whereas solid lines (blue for NV$^-$, red for P1) represent the steady state numerical solution of the rate equations (A1) and (A2). The parameters used for the calculations are $C_O = 1.5$, $P_{zT} = -9.7 \times 10^{-3}$, $T_{1T,NV}^{-1} = 25$ Hz, $T_{1N,NV}^{-1} = 5$ Hz, $T_{1T,P1}^{-1} = 8$ Hz, $T_{1P1}^{-1,F1} = 40$ Hz and $T_{1P1}^{-1,d,F1} = 0$.

A wide range of frequencies and magnetic field amplitudes. These transitions may enable better sensitivity to magnetic field, which is a key feature in quantum sensing and quantum information. The ability to simultaneously probe the magnetic resonances of both NV$^-$ and P1 can be exploited for sensitivity enhancement by using hyperpolarization of P1 defects and exploiting the large density of P1 defects in diamond compared to NV$^-$ defects ($\sim 100$ times larger).

In addition, we observe an unknown resonance feature in the ODMR spectrum. This feature is markedly clear and is symmetric around the GSLAC magnetic field, leading us to conclude that it corresponds to coupling between NV$^-$ and another unknown resonance. A significant population inversion is observed with $B > 102$ mT.

Further study is needed to understand the mechanism responsible for the anomalous saturation and to overcome it in order to reach the threshold of masing.

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Appendix A: Rate equations

Consider the case where a transverse excitation having amplitude $\omega_1$ and angular frequency $\omega_p$ is applied to the P1 spins having angular transition frequency $\omega_{P1}$. In addition OISP is applied to the NV spins having angular transition frequency $\omega_{NV}$. The rate equations for the P1 and NV spin polarizations, which are denoted by $P_{1,P1}$ and $P_{2,NV}$, respectively, are taken to be given by

$$\frac{dP_{1,P1}}{dt} = -\frac{P_{1,P1} - P_{\omega,P1}}{T_{P1}}, \quad (A1)$$

$$\frac{dP_{2,NV}}{dt} = -\frac{P_{2,NV} - P_{\omega,NV}}{T_{NV}}. \quad (A2)$$

The P1 steady state value $P_{\omega,P1}$ is obtained by averaging the contributions of driving-induced depolarization (relevant terms are labeled by the subscript d), dipolar coupling to NV spins (subscript I) and thermal relaxation (subscript T)

$$P_{\omega,P1} = \frac{T_{d,P1}^{-1} + T_{I,P1}^{-1}P_{2,P1} + T_{T,P1}^{-1}P_{2,T,P1}}{T_{P1}^{-1}}, \quad (A3)$$

where $T_{d,P1}^{-1} + T_{I,P1}^{-1} + T_{T,P1}^{-1}$ is the total P1 rate. For the case where the P1 transverse relaxation time $T_{2,P1}$ is much shorter than the longitudinal relaxation time the driving-induced depolarization rate is given by

$$T_{d,P1}^{-1} = \frac{\omega_p^2 T_{2,P1}}{1 + (\omega_p - \omega_{P1})^2T_{2,P1}^2}. \quad (A4)$$

Similarly, the NV steady state value $P_{\omega,NV}$ is obtained by averaging the contributions of dipolar coupling to P1 spins (subscript I), thermal relaxation (subscript T) and OISP (subscript O)

$$P_{\omega,NV} = \frac{T_{d,NV}^{-1}P_{2,NV} + T_{I,NV}^{-1}P_{2,T,NV} + T_{O,NV}^{-1}P_{2,O,NV}}{T_{NV}^{-1}}. \quad (A5)$$

where $T_{NV}^{-1} = T_{d,NV}^{-1} + T_{I,NV}^{-1} + T_{O,NV}^{-1}$ is the total NV rate.

When higher states are disregarded the P1 and NV thermal polarization coefficients are given by $P_{2,T,P1} = -\tanh(\omega_{P1}/\omega_T)$ and $P_{2,T,NV} = -\tanh(\omega_{NV}/\omega_T)$, respectively, where $\omega_T = 2k_BT/h$, $h$ is the Planck’s h-bar constant and $k_BT$ is the thermal energy, and the polarization coefficients due to dipolar coupling $P_{2,I,P1}$ and $P_{2,I,NV}$ are given by

$$P_{2,I,P1} = \tanh \left( \frac{\omega_{P1}^2}{\omega_{NV}^2} \frac{1}{\omega_{P1}} \right), \quad (A6)$$

$$P_{2,I,NV} = \tanh \left( \frac{\omega_{NV}^2}{\omega_{P1}^2} \frac{1}{\omega_{NV}} \right). \quad (A7)$$

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