Prospective Acceleration of Diffusion Tensor Imaging with Compressed Sensing Using Adaptive Dictionaries

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Purpose: Diffusion MRI requires acquisition of multiple diffusion-weighted images, resulting in long scan times. Here, we investigate gate combining compressed sensing and a fast imaging sequence to dramatically reduce acquisition times in cardiac diffusion MRI.

Methods: Fully sampled and prospectively undersampled diffusion tensor imaging data were acquired in five rat hearts at acceleration factors of between two and six using a fast spin echo (FSE) sequence. Images were reconstructed using a compressed sensing framework, enforcing sparsity by means of decomposition by adaptive dictionaries. A tensor was fit to the reconstructed images and fiber tractography was performed.

Results: Acceleration factors of up to six were achieved, with a modest increase in root mean square error of mean apparent diffusion coefficient (ADC), fractional anisotropy (FA), and helix angle. At an acceleration factor of six, mean values of ADC and FA were within 2.5% and 5% of the ground truth, respectively. Marginal differences were observed in the fiber tracts.

Conclusion: We developed a new k-space sampling strategy for acquiring prospectively undersampled diffusion-weighted data, and validated a novel compressed sensing reconstruction algorithm based on adaptive dictionaries. The k-space undersampling and FSE acquisition each reduced acquisition times by up to 6× and 8×, respectively, as compared to fully sampled spin echo imaging. Magn Reson Med 76:248–258, 2016. © 2015 The Authors. Magnetic Resonance in Medicine published by Wiley Periodicals, Inc. on behalf of International Society for Magnetic Resonance in Medicine. This is an open access article under the terms of the Creative Commons Attribution License, which permits use, distribution and reproduction in any medium, provided the original work is properly cited.

Key words: diffusion MRI; diffusion tensor imaging; prospective undersampling; compressed sensing; adaptive dictionaries; heart structure

INTRODUCTION

Diffusion MRI (dMRI) is a noninvasive technique that measures the displacement of water molecules as a marker of cell orientation and integrity. In the myocardium, fiber and sheet orientation have been shown to coincide with the eigenvectors of the diffusion tensor (1,2). In diffusion tensor imaging (DTI), diffusion-weighted (DW) measurements are performed in a minimum of six directions plus one nondiffusion weighted scan, and the data are fitted with a monoexponential tensor model (3). As a result, scan times can be long, limiting the clinical application of DTI. This has led to the development of several methods for accelerating cardiac dMRI including reduced encoding sequences (4), parallel imaging (5), and simultaneous multislice imaging (6).

In recent years, compressed sensing (CS) has emerged as a popular method for reconstructing undersampled MRI data (7). The requirements for CS reconstruction of undersampled MRI data are that the images are sparse in a specific transform domain, and that the reconstruction artefacts from the transform are incoherent with those from undersampling (7).

The problem of how best to sparsify dMRI signals has been widely discussed in recent years. Several studies use wavelet transforms for sparsifying the diffusion propagator (8,9) or signal in image-space (10). Spherical ridgelets, based on wavelet theory, also offer a means to sparsely represent diffusion signals (11). Recently, Mani et al (12) proposed a compressed sensing reconstruction algorithm based on a multitensor model (13), where the diffusion signal at each voxel was modelled using contributions from a dictionary consisting of one isotropic component and several anisotropic components. However, such dictionaries were intended for application in white matter in the brain, and their suitability for the heart is unclear given the lower anisotropy of cardiac tissue (14). Adaptive dictionaries (15,16) provide a method of sparsely representing diffusion signals without making assumptions about the underlying diffusion processes.

In dMRI, undersampling may be performed in k-space (8,10,12,17–19), or in q-space (13,15,16,20–23). Q-space undersampling is generally applied when the number of diffusion-encoding directions is high, such as in high angular resolution diffusion imaging or diffusion spectrum imaging. When the number of diffusion-encoding directions is low, k-space undersampling is more commonly performed. Furthermore, a different k-space sampling scheme may be used to acquire each image volume so as to decrease coherence in data sampling (8,10,12,18).

To the best of the authors’ knowledge, previous published work accelerating DTI with CS have been limited to retrospectively undersampled data. In this work, we present and evaluate a complete system for prospectively accelerated acquisition and reconstruction of three-
dimensional (3D) DTI data, with the aim of reducing total acquisition time. The acquisition combines variable density k-space undersampling with a fast spin echo sequence. The reconstruction algorithm exploits sparsity by means of adaptive dictionaries (24,25), and incorporates T2-weighting correction. The T2-weighting correction supports fast echo-train imaging methods, and leads to greater flexibility in k-space trajectory designs. We compared retrospectively and prospectively undersampled ex vivo cardiac data, and validated the reconstructions against fully sampled data acquired during the same session. A preliminary version of this work was presented in McClymont et al (26).

METHODS

MR Setup and Acquisition

MRI was performed using a 9.4 Tesla (T) preclinical scanner (Agilent Technologies, Santa Clara, CA), a shielded gradient system (1 T/m) and a quadrature-driven transmit/receive birdcage coil of 20 mm inner diameter (Rapid Biomedical, Rimpar, Germany). Fully sampled 3D fast spin echo (FSE) DTI data were acquired with the following parameters: TR/TE = 250/9.3 ms, echo spacing = 4.9 ms, echo train length = 8, resolution = 100 μm isotropic, acquisition matrix (kx x ky x kz) = 200 x 160 x 160, field-of-view = 20 x 16 x 16 mm, number of non-DW images = 8, number of DW directions = 61, diffusion duration (D) = 2 ms, diffusion time (Δ) = 5.5 ms, b-value = 1000 s/mm², acquisition time = 15 h 20 m. The receiver gain was optimized for DW and non-DW scans. Noise data were acquired using an identical sequence, without radiofrequency (RF) pulses and with TR = 67 ms.

Prospectively undersampled data were acquired at 2x, 3x, 4x, 5x, and 6x acceleration factors, with a different randomized undersampling mask for each image volume. The parameters used were identical to the fully sampled data, with the following differences: number of non-DW images = 4, number of DW directions = 30. The diffusion scheme used here corresponded to the first 30 of 61 DW directions of the fully sampled data (27). The acquisition times were 3 h 46 min, 2 h 31 min, 1 h 53 min, 1 h 30 min, and 1 h 15 min, respectively. In addition, 3D
multiecho spin echo data were acquired for T2 mapping. The following parameters were used: TR/TE1 = 250/4.7 ms, echo spacing = 4.7 ms, echo train length = 16, resolution = 100 μm isotropic.

k-Space Sampling

In an FSE acquisition, the number of echoes per excitation is fixed. In the fully sampled datasets, the two phase-encoding directions k_x and k_y were traversed in a standard center-out interleaved and linear manner, respectively. This resulted in a stepped filter of equal width bands across k_y modulated by T2 relaxation. To implement the prospectively undersampled DTI sequence, a sampling scheme was generated that divides k_y into bands of variable widths, whilst maintaining a center-out phase encoding scheme to mitigate discontinuities in T2-weighting. Figure 1 illustrates the sampling schemes for both retrospectively and prospectively undersampled data. First, a probability density function (PDF) was generated in k_y; k_z for each acceleration factor, f. Following (10), this PDF was constructed using a polynomial of order f + 1, with the central 15% of k-space fully sampled. In the prospectively undersampled case, bands in k_y were defined such that the integral of the PDF in each band was approximately equal at k_z = 0. Although the same PDF was used for each imaging volume, the sampling schemes were generated independently to decrease coherence. Samples were randomly allocated based on the PDF, first in k_z and then in k_y, independently for each half of k-space (k_y > 0 and k_y ≤ 0). Each read-out (k_x) was fully sampled. The retrospectively undersampled k-space data were sampled in the same locations as the prospectively undersampled data.

Notation

Matrices and arrays are denoted using upper case bold letters; vectors are denoted using lower case bold. Images are represented interchangeably as arrays, as in I_{x,y,z,n}, or as matrices, as in I ∈ Z^{N×V} where V = X × Y × Z is the total number of voxels. X, Y, and Z refer to the dimensions of the data in the read-out and two phase encoding directions, respectively. N refers to the number of image volumes including DW and non-DW data. Elements of arrays are denoted using subscripts, such as I_{x,y,z,n}. Column v of matrix I is denoted i_v.

Image Reconstruction

Images were reconstructed using the compressed sensing framework shown in Figure 2. The input k-space data to the reconstruction algorithm were initialized using a “sliding window” approach (8,28), in which unsampled locations are filled with those of the nearest acquired diffusion direction. This was performed independently for the non-DW and DW data.

Although noise in magnitude MR images follows a Rician distribution, given a sufficiently high signal-to-noise ratio (SNR) it can be approximated as Gaussian (29). However,
the different receiver gain settings introduce heteroscedasticity between the non-DW and DW data. Therefore, data whitening must first be performed so that errors can be assumed to follow a Gaussian distribution, and can, therefore, be minimized using the computationally efficient \( \ell_2 \)-norm. The noise level at each receiver gain was computed as the standard deviation of the real component of the non-DW data in k-space. Before reconstruction, the non-DW and DW images were whitened by dividing the data in k-space by the appropriate noise level. Following reconstruction, the images were unwhitened by multiplying by the respective noise level.

The complex diffusion weighted images, \( I \subseteq \mathbb{C}^{N \times Y \times Z \times N} \), were reconstructed by solving the following optimization problem:

\[
\hat{I} = \arg \min_{I} \| \mathcal{F}(I) - Y \|^2_2 + \lambda_1 \| I \|_{TV} + \lambda_2 \| \phi(I) \|_1. \tag{1}
\]

The first term in Eq. [1] refers to data consistency, where \( Y \) denotes the whitened k-space data, and \( \mathcal{F}(I) \) is the k-space of the reconstructed image, as follows:

\[
\mathcal{F}(k_x, k_y, k_z, n)(I) = \sum_{x,y,z} I(x,y,z,n) e^{-i 2 \pi \left( \frac{k_x x}{C_0} + \frac{k_y y}{C_1} + \frac{k_z z}{C_2} \right)} e^{j \frac{2 \pi}{C_3} T_E k_y y}. \tag{2}
\]

This definition differs from the discrete Fourier transform in that it incorporates the echo time, \( T_E(k_z) \), at each phase encoding location, and the \( T_2 \) at each voxel, \( T_{2x,y,z} \). This term mitigates the ringing and blurring artefacts due to discontinuous \( T_2 \)-weighting in k-space (30,31). \( T_2 \) maps were obtained by fitting the multiecho spin echo data with a monoexponential relaxation curve using weighted linear regression. The \( T_E(1) \) term allows the approximation of the \( T_2 \) relaxation that would have occurred, had all of the data been acquired at the TE of the first echo.

The second term in Eq. [1] controls image smoothness. The total variation (TV) was computed from the magnitude of the diffusion-weighted images \( |I| \) as follows:

\[
||I||_{TV} = \sum_{x,y,z,n} ||I_{x+1,y,z,n} - I_{x,y,z,n}|| + ||I_{x,y+1,z,n} - I_{x,y,z,n}|| + ||I_{x,y,z+1,n} - I_{x,y,z,n}|| + ||I_{x,y,z,n-1} - I_{x,y,z,n}||. \tag{3}
\]

Finally, the third term in Eq. [1] controls the sparsity of the image under the transformation \( \phi \). Here, \( ||\phi(I)||_1 \) refers to the \( \ell_1 \)-norm of the linear decomposition by a dictionary, as described in the following section. Tuning parameters \( \lambda_1 \) and \( \lambda_2 \) control the relative weights of the total variation and sparsity terms.

Sparse Representation

Let \( x \subseteq \mathbb{C}^{N \times 1} \) denote the magnitude of the diffusion-weighted signal at a particular voxel. Following Gramfort et al (16), \( x \) was modeled as follows:

\[
x = Da + \varepsilon \tag{4}
\]

where \( D \subseteq \mathbb{C}^{N \times D} \) refers to the dictionary, \( a \in \mathbb{C}^{D \times 1} \) are the coefficients, and \( \varepsilon \subseteq \mathbb{C}^{N \times 1} \) is a noise term. The coefficient vector \( a \) should be sparse (i.e., use as few columns of the dictionary as possible), while minimizing the magnitude of the residuals \( \varepsilon \). Given that \( x \) is strictly nonnegative, it follows that \( D \) and \( a \) are also nonnegative (16).

Given a set of whitened training data \( X = \{x_1, \ldots, x_n\} \subseteq \mathbb{C}^{N \times Y \times Z \times N} \), the dictionary was trained as follows (25):

\[
D^*, A^* = \arg \min_{D \geq 0, A \geq 0} \frac{1}{2} \sum_{n} ||a_n||_{0} \text{ s.t. } ||x_n - Da_n||_{2} \leq N \tag{5}
\]

where \( A = [a_1, \ldots, a_n] \subseteq \mathbb{C}^{D \times Y \times Z \times N} \) contains the sparse coefficients. As the data was whitened such that the noise has a variance of 1, the residual sum of squares should be less than or equal to \( N \). To prevent \( D \) from having arbitrarily large values, its columns \( d_1, \ldots, d_0 \) are constrained to each have an \( \ell_2 \)-norm of less than or equal to one.

During reconstruction, the magnitude image \( |I| \subseteq \mathbb{C}^{N \times Y \times Z \times N} \) in Eq. [1] was \( \ell_2 \)-"norm" decomposed using iteratively re-weighted \( \ell_1 \)-norm decomposition (32,33). The decomposition was performed using the trained dictionary as follows:

\[
A^* = \arg \min_{A \geq 0} \|W A\|_1 \text{ s.t. } ||I - DA||_2 \leq \lambda \tag{6}
\]

where \( W = \frac{1}{||I||_{TV}} \). The stability parameter, \( \varepsilon \), was 0.01. Thus, \( \|W A\|_1 \approx \|A\|_1 \). The error term, \( \lambda \), was \( N \) in the first iteration of the reconstruction algorithm. In subsequent iterations, \( \lambda \) was equal to \( \sum_{i} ||I_i - DA_i||_2 \), using \( A \) from the previous iteration.

The sparsity term, \( ||\phi(I)||_1 \), in Eq. [1] is defined as \( \sum (||A||_1 + ||I - DA||_1) \). This is equivalent to representing residuals using additional columns of the dictionary, \( d_{0,1} = [1, 0, \ldots, 0]^T, \quad d_{0,2} = [0, 1, \ldots, 0]^T, \ldots, \quad d_{0,N} = [0, 0, \ldots, 1]^T \), thus maximizing their \( \ell_1 \)-norm.

Iterative Reconstruction

Nonlinear conjugate gradient descent was used to perform the reconstruction. Seventy iterations were typically sufficient for convergence. The tuning parameters \( \lambda_1 \) and \( \lambda_2 \) were 1 and 10 in the 2D phantom reconstructions, and \( 10^{-4} \) and 0.1 in the 3D ex vivo data reconstructions, respectively. The number of dictionary columns, \( D \), was 100. These parameters were empirically tuned using additional data, not included in this study. Dictionary learning and sparse decomposition was performed using the SPAMS toolbox of Mairal et al (25), using the weighted LASSO algorithm (34) for sparse decomposition. The \( \ell_0 \)-norm decomposition required only two iterations of weighted \( \ell_1 \)-norm decomposition.

In the case of the numerical phantom data, the dictionary was trained using the fully sampled (ground truth) data. In the case of the ex vivo data, dictionary training was performed for each of the five ex vivo heart samples in turn, using fully sampled data from the remaining four samples. The training data consisted of all voxels containing cardiac tissue, and 1% of the remaining voxels (randomly sampled from air, buffer, and gel). The data were whitened before training. The training was performed using orthogonal matching pursuit (35), with
200 iterations and a batch size of 512. These parameters, provided they were sufficiently large, were not found to significantly affect the dictionaries.

The reconstruction was performed in 3D using MATLAB R2013a (Mathworks, Natick, MA). For the ex vivo data, this required approximately 11 h per reconstruction on a 12 core 2.7 GHz Mac Pro, primarily due to the large number of 3D Fourier transforms associated with the $T_2$-weighting correction, as well as the sparse decomposition step.

Numerical Phantom Simulation

A 2D numerical cardiac phantom, displayed in Figure 3, was generated to evaluate the performance of the CS reconstruction. The geometry and MRI parameters of the phantom simulated a simplified left ventricle. The phantom was oriented in a short-axis view with the read-out oriented through-plane, and the two phase encoding directions oriented in-plane with an acquisition matrix of $160 \times 160$. The phantom contained three concentric annuluses corresponding to buffer, tissue, and gel. The $T_2$ values of the three components were 40, 24, and 30 ms, respectively. The diffusion in the buffer and gel components was isotropic, with diffusion coefficients of $2 \times 10^{-3}$ mm$^2$/s, respectively. The signal in the tissue component was generated based on a diffusion tensor model, whose primary, secondary, and tertiary eigenvalues were $1.3$, $1.0$, and $0.7 \times 10^{-3}$ mm$^2$/s, respectively. Thus, the mean apparent diffusion coefficient (ADC) was $1.0 \times 10^{-3}$ mm$^2$/s, and the fractional anisotropy (FA) was 0.29. The projection of the primary eigenvectors ($v_1$) in the short-axis plane had a circumferential orientation, and the helix angle (HA), as defined as the elevation angle of $v_1$ with respect to the short-axis plane, had a linear transition between $-90^\circ$ at the outer radius (subepicardium) to $90^\circ$ at the inner radius (subendocardium). The tertiary eigenvectors ($v_3$) were oriented radially. The secondary eigenvectors ($v_2$) were oriented perpendicular to $v_1$ and $v_3$. The proton density of tissue was 80% of that of the buffer and gel. Rician noise was added such that the SNR, defined as the mean divided by the standard deviation in the tissue component of the non-DW magnitude images, was 60.

Experimental Validation of Numerical Phantom Simulation

Simulated k-space data were generated for the phantom in 2D, omitting the read-out direction. $T_2$ decay was simulated according to Eq. [2] for both the retrospective and prospective sampling schemes (i.e., with both constant and variable steps in $k_y$). Next, white noise was added independently to the real and imaginary components of k-space. Finally, undersampling at acceleration factors between two and six was performed. The images were reconstructed as described above. The ground truth consisted of the phantom without noise or $T_2$ effects.

The reconstructed magnitude images were fitted with a diffusion tensor model. Parametric maps of mean ADC, FA, and HA were computed. The mean and standard deviation of the mean ADC and FA, and the root-mean-squared-error (RMSE) values of the HA difference maps were calculated. These calculations were performed for voxels corresponding to tissue only.

Animal Preparation

Hearts were excised from five Sprague-Dawley rats, weighing between 199 and 221 g, during terminal anaesthesia. Isolated hearts were swiftly perfused in Langendorff constant pressure mode at 80 mmHg with oxygenated (95% O2/5% CO2) Krebs-Henseleit buffer at 37°C (mM): NaCl 118, KCl 4.7, MgSO4.7H2O 1.2, NaHCO3 25, KH2PO4 1.2, Glucose 11, CaCl2.H2O 1.8, and arrested using high potassium cardioplegic solution. They were subsequently perfusion-fixed and immersed in isosmotic Karnovsky’s fixative with 2 mM Gadolinium contrast agent (Prohance; Bracco, MN). Experimental investigations conformed to the UK Home Office guidance on the Operations of Animals (Scientific Procedures) Act 1986 and were approved by the University of Oxford’s ethical review board.
Experimental Validation of Ex Vivo Data

The ex vivo data ground truth consisted of the fully sampled DTI data with 61 diffusion-encoding directions and 8 $b=0$ images. The retrospectively undersampled data consisted of the first 30 diffusion directions and 4 $b=0$ images. The sampling locations for the prospectively and retrospectively undersampled data were identical. However, the associated T2-weighting were different in the two schemes. Given that the image reconstruction algorithm incorporates a correction for T2-weighting during the echo train, the reconstructed prospectively undersampled data have a different profile in $k_y$ compared with the ground truth. Therefore, for comparison purposes, we applied the T2-weighting profile of the ground truth images to the reconstructed images following reconstruction, so that their T2-weighting profiles were matched. This is illustrated in Figure 4.

The magnitude images for the ground truth and undersampled data were fitted to a diffusion tensor model. The mean and standard deviation of the mean ADC and FA over all myocardial voxels for each sample is reported. The mean and standard deviation RMSE for FA over all myocardial voxels for each sample is reported. The mean and standard deviation RMSE for the three eigenvectors in the reconstructed image without T2-weighting correction. Arrows indicate regions that have been sharpened by the T2-weighting correction. The image with T2-weighting matched to the ground truth.

RESULTS

Table 1 presents the mean of the mean ADC and FA, and the RMSE of HA, in the simulated phantom for both sampling schemes. The mean ADC was underestimated by 0.8–1.1% in the retrospective scheme, and by 1.2–2.2% in the prospective scheme. The FA was underestimated by 3.2–3.9% in the retrospective scheme, and by 4.5–7.3% in the prospective scheme. The RMSE of the HA was 4.33–4.73° in the retrospective scheme, and 5.09–5.73° in the prospective scheme.

Figure 5 displays T2-matched mean ADC, FA, and HA maps in a single sample based on retrospective and prospective undersampling at acceleration factors of two and six. In general, the retrospectively undersampled reconstructed images were visually sharper than the prospectively undersampled reconstructed images. The images became increasingly unsharpened with increased acceleration.

As per the phantom experiments, FA was underestimated as a result of the prospective undersampling and reconstruction. Table 2 presents the mean and standard deviation of the mean ADC and FA over all voxels in the myocardium for prospectively undersampled data. At an acceleration factor of two, the mean ADC was approximately 0.5% higher, and the FA was approximately 2.5% lower, than the ground truth. At an acceleration factor of six, the mean ADC was approximately 1% lower, and the mean FA was approximately 5% lower, than the ground truth. The standard deviation of both parameters also decreased with increased acceleration.

In the retrospectively undersampled data, the mean RMSE of the mean ADC over the five samples was $2.4 \times 10^{-5}$ mm²/s for an acceleration factor of two, increasing to $5.2 \times 10^{-5}$ mm²/s at an acceleration factor of six. The mean RMSE of the FA was 0.014 for an acceleration factor of two, and 0.023 for an acceleration factor of six. The mean RMSE of the HA was 3.1° for an acceleration factor of two, and 4.9° for an acceleration factor of six. Joint histograms of mean ADC, FA, and HA at 6× acceleration are shown in Figure 6. The spread of the data is larger for all parameters in prospectively undersampled data, and increases with acceleration. Figure 6 also displays the RMSE values for mean ADC, FA, and HA. These data are also presented in Table 2 for the prospectively undersampled data, as is the COU values for the three eigenvectors.
The RMSE values of the prospectively undersampled data were higher than those of the retrospectively undersampled data. The mean RMSE of the mean ADC was $1.01 \pm 0.04$, $1.01 \pm 0.05$, $1.01 \pm 0.05$, $1.01 \pm 0.05$, and $1.01 \pm 0.05$ for acceleration factors of two and six, respectively. The mean RMSE of the FA was $0.28 \pm 0.02$, $0.28 \pm 0.02$, $0.28 \pm 0.03$, $0.28 \pm 0.03$, and $0.28 \pm 0.03$ for factors of two and six, respectively. The mean RMSE of the HA was $4.33$, $4.34$, $4.52$, $4.63$, and $4.73$ for factors of two and six, respectively.

Although the RMSE for mean ADC, FA, and HA increases with acceleration factor, the cones of uncertainty for all three eigenvectors decreased for acceleration factors of three or greater. Wild bootstrapping yielded 95% COU in $v_1$ of $4.7^\circ$ and $3.0^\circ$ at acceleration factors of two and six, respectively, in the prospectively sampled data, and $3.7^\circ$ in the ground truth data. The COU in $v_2$ was $19.4^\circ$ and $12.3^\circ$ at factors of two and six, respectively, and $14.7^\circ$ in the ground truth data. The COU in $v_3$ was $19.0^\circ$ and $12.0^\circ$ at factors of two and six, and $14.4^\circ$ in the ground truth data.

Regional analysis showed that the RMSE in the LV was lower than the RV. At an acceleration factor of two and in a midventricular slice, the mean ADC RMSE in the LV was $31\%$ lower, the FA RMSE was $17\%$ lower, and the HA was $47\%$ lower than the RV. At an

![Parameter maps of mean apparent diffusion coefficient (ADC), fractional anisotropy (FA) and helix angle (HA) at acceleration factors of 2 and 6 for retrospectively and prospectively undersampled data with matched T2-weighting.](image-url)
Table 2
Mean and RMSE of Mean ADC, FA, HA, and 95% Cones of Uncertainty for Acceleration Factors between Two and Six for Prospectively Undersampled T2w-Matched Data*

| Parameter                          | Ground truth | 2        | 3        | 4        | 5        | 6        |
|------------------------------------|--------------|----------|----------|----------|----------|----------|
| Mean ADC (×10⁻³ mm²/s)             | 1.07 ± 0.02  | 1.07 ± 0.02 | 1.07 ± 0.02 | 1.07 ± 0.02 | 1.07 ± 0.02 | 1.07 ± 0.02 |
| Mean FA                            | 0.26 ± 0.01  | 0.26 ± 0.01 | 0.26 ± 0.01 | 0.25 ± 0.01 | 0.25 ± 0.01 | 0.25 ± 0.01 |
| ADC RMSE (×10⁻⁵ mm²/s)             | -            | 3.78 ± 0.17 | 4.84 ± 0.17 | 5.57 ± 0.17 | 6.14 ± 0.17 | 6.64 ± 0.16 |
| FA RMSE (×10⁻²)                    | -            | 2.24 ± 0.06 | 2.85 ± 0.19 | 2.83 ± 0.12 | 3.00 ± 0.11 | 3.16 ± 0.13 |
| HA RMSE (°)                        | -            | 4.96 ± 0.44 | 5.70 ± 0.43 | 5.99 ± 0.50 | 6.40 ± 0.64 | 6.61 ± 0.66 |
| v₁ COU (°)                         | 3.7 ± 0.2    | 4.7 ± 0.2  | 2.9 ± 0.3  | 2.9 ± 0.2  | 3.0 ± 0.2  | 3.0 ± 0.3  |
| v₂ COU (°)                         | 14.7 ± 1.0   | 19.4 ± 1.4 | 12.1 ± 1.4 | 12.1 ± 1.3 | 12.3 ± 1.3 | 12.3 ± 1.4 |
| v₃ COU (°)                         | 14.4 ± 1.0   | 19.4 ± 1.5 | 11.8 ± 1.5 | 11.8 ± 1.4 | 12.1 ± 1.4 | 12.0 ± 1.4 |

*Mean and standard deviation are reported over five hearts.

Figure 7 illustrates fiber tracking in the whole heart based on v₁, v₂, and v₃. Fiber tracts based on v₁ in each undersampled case were virtually indistinguishable from the ground truth data. Smoothing of v₂ and v₃ tracts are prominent in the zero-filled retrospectively undersampled data. In contrast, v₂ and v₃ tracts were well preserved in the CS-reconstructed cases, with marginal differences in the lateral wall of the midaxial myocardium.

DISCUSSION

In this work, a novel dictionary-based approach is proposed and evaluated for accelerating DTI. Prospective undersampling up to a factor of 6× was performed,

![Image of Table 2 and Figure 7](Image Link)
reducing the total acquisition time from 7 h 30 min to 1 h 15 min. Furthermore, the correction of artifacts arising from discontinuous T2-weighting is incorporated into the reconstruction algorithm.

We observed that the prospectively undersampled data had higher errors than the retrospectively undersampled data. Our simulations show that this arises from the difference in T2-weighting between the two schemes. As a result of the narrower grouping of the initial echoes about the center of k-space in the prospectively undersampled data, its SNR is lower than that of the retrospectively undersampled data. The corollary is that for echo train imaging sequences, additional shots and time would be required to provide the same T2-weighting as the retrospectively undersampled data. Therefore, it is more accurate to state that the SNR in retrospectively undersampled data is artificially enhanced. While for single-echo imaging sequences such as a spin or stimulated echo sequences variable T2-weighting is not an issue, these sequences require significantly longer acquisition times (e.g., factor of 8 in this case).

The variable band spacing in our prospective undersampling scheme increasingly unsharpened the point spread function as the acceleration factor increased. The T2-weighting correction compensates for this and amplifies the edges of k-space. This leads to sharper but noisier images and truncation artefacts. However, these artefacts are mitigated by the total variation (image smoothness) component of the reconstruction algorithm.

Acquiring a T2 map added 1 h 46 min to the total scan time. It has been shown that discontinuous T2-weighting in fast spin echo can be corrected using only a single excitation, adding just seconds to the scan time (31). However, this approach assumes that the data in each echo train can be characterized by a single T2, and is better suited for homogeneous samples. Alternatively, acquiring a lower resolution T2 map should suffice, thus reducing the scan time overhead. In the absence of a T2 map, the T2-weighting correction can be omitted from the reconstruction algorithm, yielding images with the same T2-weighting as the acquired data. However, in this work it was necessary to correct the T2-weighting to compare the reconstructed images with the ground truth.

Comparing the RMSE values for the retrospectively undersampled reconstructions with those from a recent distributed compressed sensing study using the wavelet transform (10), we found that our mean RMSE values were 60% lower for FA and 30% lower for HA. The mean RMSE values for mean ADC were comparable in both studies. We note, however, that the mean ADC in

![FIG. 7. Fiber tracking in a 5-voxel-thick mid-myocardial axial slab based on the 1̈, 2̈, and 3̈ eigenvectors (v1, v2, and v3; top, middle, bottom). Tracts were reconstructed from ground truth data, zero-filled retrospectively undersampled data, CS-reconstructed retrospectively undersampled data, and CS-reconstructed prospectively undersampled data (left to right). In the undersampled images, the acceleration factor was 6. Tracts based on v1 were virtually indistinguishable in each case. While significant smoothing of v2 and v3 tracts were observed in the tracts reconstructed using the zero-filled data, these tracts were well preserved in the CS-reconstructed data when compared with the ground truth. Marginal differences observed in the lateral wall are highlighted with arrows.](image-url)
Reduced Acquisition Times in Cardiac Diffusion MRI

the samples of (10) were considerably lower (< 50%) than the mean ADC reported in this study, and thus the mean RMSE as a proportion of the mean ADC was also lower using our approach. The differences in mean ADC may have stemmed from differences in sample preparation, such as the fixative used and the ambient temperature.

Regarding the mean values of tensor parameters over the myocardium, the mean ADC was relatively robust to acceleration, being underestimated in prospectively 6× undersampled data by approximately 2.5%. The fractional anisotropy were less robust to acceleration, being underestimated by approximately 5%. This bias was also observed in the simulated phantom reconstructions, and is most likely a result of the dictionary not being sufficiently flexible in describing anisotropic diffusion at a range of orientations. Future research will focus on optimal representation of diffusion signals using dictionaries. Furthermore, the system would be more practical without the requirement of external training data. Dictionary training based on undersampled data will also be investigated in future work.

The 95% COU values for the reconstructed data were low, indicating a high level of precision. The COU values for an acceleration factor of two were higher than those of the ground truth data, possibly as a result of the T2-weighting correction amplifying high frequency data. At acceleration factors of three to six, the compressed sensing reconstruction has a de-noising effect, yielding lower COU values than the ground truth.

Regional analysis showed that the reconstruction performance in the left ventricle was better than in the right ventricle. One reason for this is that the LV is larger than the RV, and less susceptible to partial voluming. The loss of high frequency data will, therefore, have a greater impact on reconstruction of the right ventricle. In addition, the 95% COU in v1 is higher in the RV than in the LV. The reconstruction of the LV in the midventricular ROI was better than in the apical or basal ROIs. The midventricular LV ROI also had the lowest 95% COU in v1. This could be related to the higher SNR at the center of the RF coil.

The fiber tracking results indicate that tracking of v1 is relatively robust to undersampling, even with simple zero-filling. On the other hand, v2 and v3 are harder to reliably measure. Here, CS-reconstruction of both retrospectively and prospectively undersampled data reconstructed with CS show excellent agreement in v1, v2, and v3 tracts compared with the ground truth.

Although the diffusion tensor model was fit in this work, the sampling scheme and reconstruction pipeline is not limited to diffusion tensor imaging. The algorithm reconstructs diffusion-weighted images without fitting an explicit model of diffusion to the data. Therefore, this algorithm could be used to reconstruct data with a higher number of samples in q-space, such as in diffusion spectrum imaging.

CONCLUSIONS

A novel system for accelerating DTI that combines a fast imaging sequence with compressed sensing was implemented. This was achieved using a variable density phase encoding scheme for undersampling 3D FSE data, and a compressed sensing framework incorporating adaptive dictionaries and T2-weighting correction for reconstruction of undersampled DTI data. We acquired DTI data prospectively undersampled in k-space by up to a factor of 6. This combined with an echo train length of 8 to reduce effective scan times by up to 48 x as compared to fully sampled spin echo imaging. The quality of reconstructions of undersampled data compared favorably to the literature, and the reconstructed parameter maps and fiber tracking were in good agreement with the ground truth data. The combination of echo train sequences and compressed sensing can dramatically reduce acquisition times in DTI, and this could lead to improvements in spatial resolution, flexibility in diffusion schemes, and clinical feasibility.

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