Reevaluation of the parton distribution of strange quarks in the nucleon

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(Dated: June 16, 2014)
An earlier extraction from the HERMES experiment of the polarization-averaged parton distribution of strange quarks in the nucleon has been reevaluated using final data on the multiplicities of charged kaons in semi-inclusive deep-inelastic scattering obtained with a kinematically more comprehensive method of correcting for experimental effects. General features of the distribution are confirmed, but the rise at low $x$ is less pronounced than previously reported.

PACS numbers: 13.60.-r, 13.88.+e, 14.20.Dh, 14.65.-q

Keywords: Parton, strange quark, parton distribution

The parton distribution functions (PDFs) of the strange quarks in the nucleon describe important features of the structure of the quark sea, and constrain models of its origin [1–4]. In addition, the strangeness content of the nucleon is of interest because of its impact on calculations of short-distance processes at high energies [5], and also in view of recent ATLAS results [6], which suggest that at small $x$ it could be substantially larger than previously assumed. In 2008 HERMES published the results of the extraction of the momentum and helicity density distributions of the strange sea in the nucleon from charged-kaon production in deep-inelastic scattering (DIS) on the deuteron [7]. The shape of the polarization-averaged distribution in $x$, where $x$ is the dimensionless Bjorken scaling variable, was observed to be softer than that of the average of the $\bar{u}$ and $d$ quarks. The helicity distribution was found to be compatible with zero in the region of measurement $0.02 < x < 0.60$.

HERMES has finalized the extraction of multiplicities for each charged state of $\pi^\pm$ and $K^\pm$ [8]. In the extraction, the correction for acceptance, kinematic smearing, losses due to decay in flight and secondary strong interactions, and radiative effects is accomplished by means of a smearing matrix which is generated with a Monte Carlo simulation. The procedure is described in detail in Ref. [8]. The data of Ref. [7] were obtained by carrying out the unfolding to correct for these effects in only one dimension, $x$. Further study of the unfolding procedure has revealed that using a multi-dimensional unfolding in $x$, $z$, and $P_{h\perp}$ results in significant changes in the final multiplicities. Here $z \equiv E_h/\nu$ with $\nu$ and $E_h$ the energies of the virtual photon and of the detected hadron in the target rest frame, respectively, and $P_{h\perp}$ is the transverse momentum of the hadron with respect to the virtual-photon direction. The results for the final multiplicities [8] were obtained with this improvement and with the elimination of a requirement, used in earlier extractions, that the hadrons have momenta greater than 2 GeV. In practice, multiplicities are not defined with such a limit on the integration over the hadron momentum. The purpose of this brief note is to update the extraction of the strange-quark PDF $S(x) \equiv s(x) + \bar{s}(x)$ by employing the final HERMES multiplicities obtained by this advanced analysis. The extraction is carried out in leading logarithmic order (LO) in the strong coupling constant of quantum chromodynamics. While a next-to-leading order (NLO) extraction would be preferred, such a procedure using semi-inclusive DIS data is not currently available. However, because of the wide interest in shape and magnitude of $S(x)$, a LO extraction is an important first step.

In the isoscalar method used in the HERMES measurement, the distribution in $x$ of the strange-quark sea is extracted from the spin-averaged kaon, $K = K^+ + K^-$, multiplicity for the DIS of positrons/electrons by a deuteron target [7]. For the isoscalar deuteron, in LO this observable depends on the PDFs $S(x)$ and $Q(x) \equiv u(x) + \bar{u}(x) + d(x) + \bar{d}(x)$. Technical details of the experiment and the principles of the procedure for extracting the density distributions for these quantities are presented in Ref. [7]. The extracted kaon multiplicity is shown in Fig. 1 as a function of $x$ at the corresponding average $Q^2$ of each bin.

The multiplicity presented in Fig. 1 is the starting point for the extraction of $S(x, Q^2)$, and can be used in the future, e.g., for NLO analyses. Here we update the extraction of $S(x, Q^2)$ which is based on a number of simplifying assumptions, i.e., LO and leading twist, as

![FIG. 1. The multiplicity of charged kaons in semi-inclusive DIS from a deuteron target, as a function of Bjorken $x$. The continuous curve is calculated from the strange-quark contribution taken from the fit in Fig. 3, together with the non-strange contribution as extracted from the high-$x$ multiplicity data (see text). The green dashed (magenta dash-dotted) curve shows separately the nonstrange–(strange–) quark contribution to the multiplicity for that fit. The blue-dotted curve is the LO prediction obtained with CTEQ6L PDFs and fragmentation functions from [9]. The values of $\langle Q^2 \rangle$ for each $x$ bin are shown in the lower panel. The band represents systematic uncertainties.](image-url)
well as on fixing the fragmentation functions and PDFs to a specific set. As in the analysis reported earlier, both $S(x, Q^2)$ and the quantity $\int D^S_K(z, Q^2)dz$ are taken as unknown, and the analysis is carried out extracting their product. Here, $\int D^S_K(z, Q^2)dz$ is the integral over the measured region of $z$ of the fragmentation function describing the number density of charged kaons from a struck quark of flavor $S$, with $D^K_S(z) \equiv 2D^S_s(z)$ by charge conjugation symmetry. The relationship between this product and the kaon multiplicity is given in LO by [7]

$$\frac{dN^K(x, Q^2)}{dN^{DIS}(x, Q^2)} = \frac{Q(x, Q^2)\int D^S_K(z, Q^2)dz + S(x, Q^2)\int D^K_S(z, Q^2)dz}{5Q(x, Q^2) + 2S(x, Q^2)}.$$  

(1)

An absence of $x$ dependence shown by the HERMES data above $x > 0.1$ requires that $dS(x)/dQ(x)/dx$ vanish. This indicates that either $S(x) = 0$ or $S(x) = kQ(x)$ where $k$ is a constant. $S(x)$ is not expected to have the same shape as $Q(x)$, and all PDF reference data sets published to date are consistent with this expectation. Therefore for $x > 0.1$ it is concluded that $S(x, Q^2) \approx 0$.

In the limit $S(x, Q^2) \rightarrow 0$, for a deuteron target the multiplicity $dN^K(x, Q^2)/dN^{DIS}(x, Q^2) = \int D^S_K(z, Q^2)dz/5$ (see Eq. 1). For $x > 0.1$ the multiplicity measured by HERMES is almost constant at a value of about 0.1. The value of the multiplicity throughout this region provides a direct estimate of $\int D^K_Q(z, Q^2)dz$. To account for any residual dependence on $Q^2$ or, because of the correlation between $x$ and $Q^2$, equivalently on $x$, a first-degree polynomial was fitted to the multiplicity for $x > 0.1$ yielding the result $\int D^K_Q(z, Q^2)dz = (0.102 \pm 0.002) + (0.013 \pm 0.010)x$, as shown by the green dashed curve in Fig. 1. In the region near $x=0.13$, where $Q^2 \approx 2.5$ GeV$^2$, this fit gives the result $\int D^K_Q(z, Q^2)dz = 0.514 \pm 0.010$, compared to the value $0.435 \pm 0.044$ obtained for $Q^2 = 2.5$ GeV$^2$ from a global analysis of fragmentation functions [9]. The weak $x$ dependence obtained in the fit is consistent with the $Q^2$ dependence exhibited by the results of the global analysis.

To assess the impact of the more accurate estimate of $\int D^K_Q(z, Q^2)dz$ resulting from the HERMES data an extraction of $S(x, Q^2)$ was made using the fragmentation functions from the global analysis of [9]. The results, presented in Fig. 2, have an $xS(x, Q^2)$ with large uncertainties in the high-$x$ region, and demonstrate the importance of a more precise value for $\int D^K_Q(z, Q^2)dz$ as is that extracted from the analysis reported here.

The extracted quantity $\int D^S_K(z, Q^2)dz$ was used together with values of $Q(x, Q^2)$ from CTEQ6L [11] and the measured multiplicity to obtain the product $S(x, Q^2)\int D^S_K(z, Q^2)dz$. As in Ref. [7], the contribution of the strange quarks to the denominator in Eq. 1 was initially neglected leading to

$$S(x, Q^2)\int D^S_K(z, Q^2)dz \simeq (2)$$

$$Q(x, Q^2)\left[5 \frac{dN^K(x, Q^2)}{dN^{DIS}(x, Q^2)} - \int D^K_Q(z, Q^2)dz\right].$$

A small iterative correction was then made to account for the neglect of this term.

The result for the product $S(x, Q^2)\int D^S_K(z, Q^2)dz$ together with a fit of the form $x^{-a_1}e^{-x/a_2}(1-x)$ are shown in Fig. 3. In the region $x < 0.1$ the values of the product are substantially smaller than those reported previ-
Due to the anti-correlation of strange and non-strange kaon fragmentation functions in a global analysis, a proper consideration of the non-strange kaon fragmentation function obtained here may lead to a considerably smaller strange kaon fragmentation function. Such a revision can be expected in the next global analysis, with the result that the strange distribution as extracted here may increase.

As in the earlier extraction, the normalization of the HERMES points is determined by the value of \( \int D_{S}^{K}(z, Q^2)dz = 1.27 \). But still, the qualitative features of the shape of \( xS(x, Q^2) \) are strikingly different from the shape of \( xS(x, Q^2) \) obtained with CTEQ6L and other global QCD fits of LO PDFs as well as that of the sum of the light antiquarks. The absence of strength above \( x \approx 0.1 \) is clearly discrepant with CTEQ6L. While, in principle, the new values for the kaon multiplicities and fragmentation integrals reported here could significantly alter the results of the strange-quark helicity-distribution extraction reported in Ref. [7], in fact, their use produces no significant change in the helicity distribution reported there.

In conclusion, a new extraction of the multiplicities for charged kaons in DIS has been made and the extraction of the distribution of strange quarks in the nucleon has been reevaluated using these new data. In the measured range of \( x \), the strength of the polarization-averaged PDF \( S(x, Q^2) \) is, under the same assumptions, substantially less than reported in [7], but the shape is similar, and the momentum density is softer than that determined from the analysis of other experiments.

**ACKNOWLEDGEMENTS**

We warmly thank Juan Rojo for his efforts in generating an unpublished NNPDF2.3LO PDF data set that includes the kinematic region of the HERMES experiment, and we gratefully acknowledge the DESY management for its support, the staff at DESY and the collaborating institutions for their significant effort, and our national funding agencies for financial support.

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