**Research Article**

**Grey Prediction Model for Drying Shrinkage of Cement Concrete Made from Recycled Coarse Aggregate Containing Superabsorbent Polymers**

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The aim of this paper is to investigate the effect of superabsorbent polymers (SAPs) on the drying shrinkage of the recycled concrete (RC). The natural aggregate (NA) was replaced by recycled aggregate at three replacement ratios (0%, 50%, and 100%). Then, the recycled concrete (RC) with different SAP contents was prepared. The performance of recycled concrete with different SAP content was analyzed with slump test, compressive strength test, and drying shrinkage test. GM(1,N) grey prediction model was utilized to predict the drying shrinkage of recycled concrete containing SAP. The results show that the strength and durability of concrete are decreased by the addition of recycled aggregate. With the increase of the dosage of SAP, the strength and durability also raise. The prediction GM(1,N) model for the drying shrinkage of recycled concrete with SAP is in good agreement with the actual drying shrinkage.

**1. Introduction**

Due to low cost, convenience, simple production process, and excellent mechanical and durability properties, natural concrete (NC) materials are widely utilized in building construction, road engineering, and bridge engineering [1–4]. With the rapid development of the economy, the huge demand for concrete materials is increasing. The cement concrete is composed of cement, aggregate, sand, and some admixtures. The main source of the coarse aggregate is crushed natural rocks obtained from natural mountains [5]. This has consumed the amount of natural rock of nonrenewable resources and caused the higher price of natural aggregates. On the other hand, according to the statistics of China, the production of concrete reached 1.8 billion tons in 2020, and construction waste such as waste concrete from the demolition of abandoned buildings was approximately $1.34 \times 10^8$ tons [6–8]. Meanwhile, the construction and demolition waste (CDW) in China has shown an increasing trend.

Many studies have shown that the utilization of recycled coarse aggregate to prepare cement concrete not only saves 60% natural aggregate resource but also consumes a large amount of CDW and reduces 20% emission of CO$_2$ [9, 10]. However, replacing natural aggregates with recycled aggregates will result in a decrease in the durability of concrete. Recycled aggregate is composed of natural aggregate and old mortar. There are a lot of pores in the old mortar and interfacial transition zone (ITZ). Therefore, RA showed higher porosity and water absorption compared with natural aggregate [11]. Concrete made of RA is easy to shrink and crack, resulting in the insufficient durability of concrete. Therefore, it is necessary to investigate the shrinkage of recycled concrete. The factor that affects shrinkage is complex, including wind speed, constituents, temperature, curing time, and pore size distribution [12]. The loss of water of the calcium silicate hydrates (CSHs) caused by a low relative humidity environment usually leads to the volume reduction of concrete. This phenomenon is called drying.
shrinkage [13]. The models that are widely utilized to predict shrinkage including the EC2-08 [14], ACI 209R [15], the Bažant-Baweja B3 [16], the CEB Model Code 99 [17], and the GL2000 [18] have been improved. Haejin et al. [19] investigated dry shrinkage of crushed returned concrete aggregate, evaluated the validity of the ACI 209 model, and found that the ACI 209 model is not suitable for the mixture that is beyond the standard conditions. Therefore, a new model was established to evaluate the drying shrinkage of the concrete made from the crushed returned concrete aggregate. Al-Manaseer et al. [20] estimated the shrinkage prediction capabilities of models based on the RILEM database [21, 22] and found that the Bažant-Baweja B3 and GL2000 models convey the best predictions for the shrinkage strain. Zhang et al. [23] proposed a prediction model for early-age shrinkage of cement paste considering the influence of wind speed. Li et al. [24] established some prediction equations by analyzing the relationship between pore structure and shrinkage of cement-based materials. Wang et al. [25] established a theoretical drying shrinkage model for RC considering the properties of the concrete, including its service time and strength. Compared with the empirical statistical regression method, autoregressive moving average model, and adaptive control Markov model, the grey model is more used due to the high prediction accuracy [26]. Wang et al. [27] used GM (1, 1) model to predict the drying shrinkage of crumb rubber concrete. Tang et al. [28] established the monthly attenuation prediction for asphalt pavement performance by using GM (1, 1) model. Shrinkage is one of the important factors that affect the durability of recycled concrete, which is closely related to time. However, there are few studies on the grey prediction model for shrinkage of concrete made from recycled aggregates.

The internal curing material maintains the relative humidity inside the concrete by releasing water, and it was used in cement concrete to solve the problem of shrinkage and cracking. As a highly effective internal curing material, superabsorbent polymers (SAPs) can significantly decrease the shrinkage of concrete. Kong et al. [29] analyzed the influence of presoaked SAP on the shrinkage of high-performance concrete (HPC) and found that the addition of SAP decreased the drying shrinkage of high-performance cement-based materials under the same water-cement ratio. Ma et al. gained a similar result. In this study, NA is replaced by RA with 0%, 50%, and 100% replacement rates. Recycled aggregate concretes with 0.3%, 0.5%, and 0.7% SAP were prepared. The workability, mechanical properties, and shrinkage of concrete made from recycled coarse aggregate containing were analyzed, respectively. GM (1, N) grey prediction model was established to predict the drying shrinkage of recycled concrete with SAP.

2. Materials and Methods

2.1. Raw Materials. Ordinary Portland cement was utilized in this paper and its physical properties are shown in Table 1. Recycled coarse aggregate was used in the experiments with the grain size of 4.75–9.5 mm, 9.5–19 mm, and 19–31.5 mm. The physical properties of recycled coarse aggregate are shown in Table 2. River sand was used as fine aggregate, and its properties are shown in Table 3. Superplasticizer was supplied by Shandong Gaoqiang Co., Ltd., and its solid content was 37%. The performance of SAP is shown in Table 4.

2.2. Preparation of Recycled Concrete with SAP. The recycled aggregate was adopted by weight of natural aggregate at 0%, 50%, and 100%. The proportions of recycled concretes are shown in Table 5. The content of SAP is set as 0%, 0.3%, 0.5%, and 0.7% by mass of concrete.

2.3. GM (1, N) Grey Prediction Model. The grey theory is a kind of prediction method that can predict, make decision, or control using incompleteness of information. As the system is whitened by many effective messages around its forecast origin, the predicted series is fairly good.

Pairs of observations \( \{x_1^{(0)}(1), x_1^{(0)}(2), \ldots, x_1^{(0)}(n)\} \) from a certain dynamic system with \( n-1 \) inputs \( \{x_2^{(0)}, x_3^{(0)}, \ldots, x_n^{(0)}\} \) and an output \( x_1^{(0)} \) are supposed to be available at an equispaced interval of time. Consider the original series, it can be obtained that

\[
X_1^{(0)} = \{x_1^{(0)}(1), x_1^{(0)}(2), \ldots, x_1^{(0)}(n)\},
\]

\[
X_2^{(0)} = \{x_2^{(0)}(1), x_2^{(0)}(2), \ldots, x_2^{(0)}(n)\},
\]

\[
X_N^{(0)} = \{x_N^{(0)}(1), x_N^{(0)}(2), \ldots, x_N^{(0)}(n)\}.
\]

\( X_i^{(1)} \) are the 1-AGO series of \( X_i^{(0)} \), \( i = 1, 2, \ldots, N \), respectively. In addition, \( Z_i^{(1)} \) is the adjacent generated serial of \( X_i^{(1)} \), and then

\[
x_1^{(0)}(k) + aZ_1^{(1)}(k) = \sum_{i=2}^{N} x_i^{(1)}(k)
\]

is called the grey differential equation of GM (1, N) model, where \( 1 \) stands for the first-order derivative of 1-AGO series of \( X_i^{(0)} \) (called the predicted series) and \( n \) stands for there being \( n-1 \) relative series (called the associated series) of the system.

Define \( \tilde{\alpha} = [a \ b_2 \ \cdots \ b_N]^T \) as the parameter series of the grey differential equation of GM (1, N) model, and then according to the least square method (LSM), it can be obtained that

\[
\tilde{\alpha} = (B^T B)^{-1} B^T Y,
\]

where

\[
B = \begin{bmatrix}
-z_1^{(1)}(2) & x_2^{(1)}(2) & \cdots & x_N^{(1)}(2) \\
-z_1^{(1)}(3) & x_2^{(1)}(3) & \cdots & x_N^{(1)}(3) \\
\vdots & \vdots & \ddots & \vdots \\
-z_1^{(1)}(n) & x_2^{(1)}(n) & \cdots & x_N^{(1)}(n)
\end{bmatrix},
\]

and

\[
Y = \begin{bmatrix}
x_1^{(1)}(1) \\
x_1^{(1)}(2) \\
\vdots \\
x_1^{(1)}(n)
\end{bmatrix}.
\]
Therefore, the approximate time response equation of equation (4) can be derived as

$$x_1^{(1)}(t) = e^{-at} \left[ \sum_{i=2}^{N} b_i x_1^{(i)}(t)e^{at} dt + x_1^{(0)}(0) - \sum_{i=2}^{N} b_i x_1^{(i)}(0)dt \right].$$

Then

$$\frac{dx_1^{(1)}}{dt} + ax_1^{(1)} = b_2 x_2^{(1)} + b_3 x_3^{(1)} + \cdots + b_N x_N^{(1)},$$

is the albinism differential equation or silhouette equation of equation (4). From equation (8), the modeling value can be derived as

$$x_1^{(1)}(k+1) = x_1^{(0)}(0) - \frac{1}{a} \sum_{i=2}^{N} b_i x_i^{(i)}(k+1) e^{at} + \frac{1}{a} \sum_{i=2}^{N} b_i x_i^{(i)}(k+1),$$

where $x_1^{(1)}(0)$ is equal to $x_1^{(0)}(1)$. Then

$$x_1^{(0)}(k+1) = x_1^{(1)}(k+1) - x_1^{(1)}(k).$$

### 2.4. Test Procedure

#### 2.4.1. Slump Test

Slump test was widely utilized to estimate the fluidity and working performance of concrete, and the operation was in accordance with specification (GB/T50081-2002, 2002; ASTM C143–C143M-15a, 2015).

#### 2.4.2. Compressive Strength Test

According to the specification (GB/T50081-2002, 2002; ASTM C39/C39M-18, 2018a), the universal testing machine (UTM) was carried out to examine the compressive strength of 3 days, 7 days, and 28 days at the loading speed of 0.8 MPa/s.
2.4.3. Drying Shrinkage. The drying shrinkage samples of RC with 100 mm × 100 mm × 400 mm were prepared. After took away the model, the sample was stored in a dry room under the condition of 20°C and 50% relative humidity (RH). The change of length at 1, 3, 7, 14, 28, 56, and 90 days was estimated by shrinkage measuring instrument. Every type of concrete should be prepared as three samples, and the average value is reported as the results.

3. Results and Discussions

3.1. Slump of Concrete. The slump and expansion of fresh concrete are shown in Figure 1. When the SAP content is 0%, the slump and expansion of concretes decrease with the increase of the replacement proportion of RA. This is because the RA contained many inherent defects and microcracks and was covered by old mortar. The old mortar causes the increase of water absorption of RA and reduces the slump and expansion of recycled concrete. When the replacement proportion of RA is the same, the slump and extension of recycled aggregate increase with the increase of SAP dosage. A possible explanation for this might be that SAP is a microsphere, which can reduce the friction resistance among aggregates and improve the expansion and slump of the recycled concrete.

3.2. Compressive Strength. Figure 2 shows the influence of SAP on the compressive strength of recycled concrete. It can be seen that the compressive strength of concrete decreases with the increase of the replacement proportion of RA. When the replacement proportion of RA is 100%, the compressive strength (7d and 28d) of recycled concrete with SAP decreases. However, the reduction value of compressive strength of recycled concrete with SAP is smaller than that without SAP. This indicates that the addition of SAP can improve the mechanical properties of recycled concrete. Meanwhile, with the rise of SAP content, the compressive strength of recycled concrete becomes higher.

The RA contained many inherent defects and microcracks and was covered by old mortar, which leads to the decrease of modulus of elasticity. When added to recycled aggregate concrete, the SAP can reduce the amount of mixing water and the water-cement ratio. This is one reason that SAP can enhance the strength of concrete.

In addition, when the hydration process of cement consumes internal water of concrete, SAP will release the water that is absorbed to promote the hydration process of cement-based materials. Therefore, the hydration time of recycled concrete incorporation with SAP is longer than that without SAP, so its mechanical property is improved.

3.3. Shrinkage of Concrete. Figure 3 shows the effect of SAP content on the drying shrinkage rate of recycled concrete. It can be seen that the drying shrinkage rate of recycled concrete develops rapidly in the early stage and grows slowly in the later stage. With the rise of the replacement amount of RA, the drying shrinkage rate of concrete also raises. Under the condition of the same age and replacement amount of RA, the shrinkage rate of the recycled concrete with different dosages of SAP is lower than that without SAP, demonstrating that the addition of SAP can effectively reduce the drying shrinkage of the recycled concrete.

The higher water absorption of RA is the reason that causes the bigger drying shrinkage of recycled aggregate. To meet the workability of recycled concrete, more water will be added. However, the mixing water could not be completely consumed by the hydration process. After hardened, the evaporation of water will leave the pore and cause the shrinkage of concrete. The SAP acts as a “reservoir” in recycling concrete. After the water evaporation, the inside of the concrete is relatively dry, and SAP will release the water that is absorbed to promote the further hydration of cement-based material.

SAP continuously supplements the evaporated water of recycled concrete. This reduces the drying shrinkage of concrete and promotes the completion of hydration of concrete. The increase of hydration products can improve the density of concrete and reduce the drying shrinkage of concrete.

4. Prediction of Recycled Concrete Shrinkage Containing SAP Based on the Grey Prediction Model

The grey prediction model is mainly aimed at the processing of equidistant data. To obtain the data with equal spacing, the dry shrinkage rate (Y) is fitted linearly. However, due to the larger value of the dry shrinkage rate (Y), it is not convenient for calculation, so the dry shrinkage rate (Y) is normalized. Then the normalization interval is adjusted to a positive value, and the dry shrinkage (Y) that suffered the above process is finally used for grey prediction. Similarly,
Figure 2: Influence of SAP on mechanical properties of reclaimed aggregate concrete. (a) 0% RA. (b) 50% RA. (c) 100% RA.

Figure 3: Influence of SAP content on drying shrinkage of recycled concrete. (a) 0% SAP, (b) 0.3% SAP, (c) 0.5% SAP, and (d) 0.7% SAP.
this operation is also performed for time (X) to obtain the
time (X) that can be used in the grey prediction model. After
the simulation, the predicted data can be inversely
processed.

The shrinkage of recycled aggregate concrete containing
SAP is predicted by the grey prediction model. 1, 3, 7, 14, 28,
56, and 90 d shrinkage results are used as the original data for
the prediction. The results indicate that the maximum dry
shrinkage occurs about 90 d.

Figures 4–7 show the test and predicted results of drying
shrinkage. The results demonstrate that the 90 d shrinkage of
RC decreases with the increase of SAP content. This indicates
that the addition of SAP is beneficial to the durability of
concrete.

The relative error, correlation, mean square deviation
ratio, and probability of small error are usually used to
evaluate the accuracy of the grey prediction model. In this
study, the C is utilized to estimate the accuracy of the model
and it can be calculated by equations (12)–(15):

\[
\overline{x} = \frac{1}{n} \sum_{k=0}^{n} x(k),
\]

\[
S_1^2 = \frac{1}{n} \sum_{k=0}^{n} [x(k) - \overline{x}]^2,
\]

\[
S_2^2 = \frac{1}{n} \sum_{k=0}^{n} [\zeta(k) - \overline{\zeta}]^2,
\]

\[
C = \frac{S_2}{S_1}.
\]

The elevated indicators of the accuracy of the grey
prediction model are listed in Table 6.

The grade of (C)-mean square deviation ratio can be
divided into four grades. All C values in this test are less than
0.1. According to Table 6, the grade is one, indicating the
model owns best accuracy.
Figure 6: The test and predicted results of concrete shrinkage with 0.5% SAP. (a) NC, (b) RC1, and (c) RC2.

Figure 7: The test and predicted results of concrete shrinkage with 0.7% SAP. (a) NC, (b) RC1, and (c) RC2.
Table 6: The elevated indicators of the accuracy of the grey prediction model.

| Grade | Relative error | Correlation | (C)-mean square deviation ratio | Probability of small error |
|-------|----------------|-------------|---------------------------------|---------------------------|
| One   | 0.01           | 0.90        | 0.35                            | 0.95                      |
| Two   | 0.05           | 0.80        | 0.50                            | 0.80                      |
| Three | 0.10           | 0.70        | 0.65                            | 0.70                      |
| Four  | 0.20           | 0.60        | 0.80                            | 0.60                      |

5. Conclusions

In this paper, the natural aggregate (NA) was replaced by recycled aggregate at three replacement ratios (0%, 50%, and 100%). Then, the recycled concrete (RC) with different SAP contents was prepared. The performance of recycled concrete with different SAP contents was analyzed by slump test, compressive strength test, and drying shrinkage test. GM (1, N) grey prediction model was utilized to predict the drying shrinkage of recycled concrete containing SAP.

1. The replacement of natural coarse aggregate with recycled aggregate has a negative influence on the workability, mechanical properties, and shrinkage of concrete.

2. With the increase of the dosage of SAP, the strength and durability of recycled concrete also raise. The proper dosage of SAP is 0.7%.

3. The prediction GM (1, N) model for the drying shrinkage of recycled concrete with SAP is in good agreement with the actual drying shrinkage. This indicates that the grey system theory is feasible to predict the drying shrinkage of recycled concrete with SAP.

4. The GM prediction model provides a new and effective way of predicting the shrinkage of concrete. In addition, more factors such as the change of climate should be considered in this model in the future study.

Data Availability

The authors would like to declare that all the data in the manuscript were obtained by experiment and the data are true and effective in the manuscript.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

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