A programmable two-qubit solid-state quantum processor under ambient conditions

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Quantum computers, which take advantage of the superposition and entanglement of physical states, could outperform their classical counterparts in solving problems with technological impact such as factoring large numbers and searching databases. A quantum processor executes algorithms by applying a programmable sequence of gates to an initialized state of qubits, which coherently evolves into a final state containing the result of the computation. Although quantum processors with a few qubits have been demonstrated on multiple quantum computing platforms, realization of solid-state programmable quantum processor under ambient conditions remains elusive. Here we report a programmable quantum processor that can be programmed with fifteen parameters to realize arbitrary unitary transformations on two spin qubits in a nitrogen-vacancy (NV) center in diamond. We implemented the Deutsch-Jozsa and Grover search algorithms with average success rates above 80%. The results pave the way to implement the programmable method in a large-scale quantum processor.

RESULTS
As depicted in Fig. 1a, the NV center consists of a substitutional nitrogen atom with an adjacent vacancy site in the diamond crystal lattice. The ground state of NV center is an electron spin triplet state with three sublevels |mS = 0⟩ and |mS = ±1⟩. A static magnetic field is applied along the NV symmetry axis ([1 1 1] crystal axis) to remove the degeneracy between the |mS = +1⟩ and |mS = −1⟩ states, yielding the electron and nuclear Zeeman splitting. The Hamiltonian of the electron spin and the 14N nuclear spin system is

$$H_{NV} = 2\pi (D S_z^2 + \omega_e S_z + Q I_z^2 + \omega_n I_z + A_{zz} S_z I_z),$$

where $S_z$ and $I_z$ are the spin operators of the electron spin (spin-1) and the nuclear spin (spin-1). The electronic zero-field splitting is $D = 2.87$ GHz and the nuclear quadrupolar interaction is $Q = -4.95$ MHz. The two spins are coupled by a hyperfine interaction $A_{zz} = -2.16$ MHz. The two-qubit quantum system is composed of $|mS = 0, mI = +1⟩, |mS = 0, mI = 0⟩, |mS = -1, mI = +1⟩, and |mS = -1, mI = 0⟩$ without considering the other spin levels. The four energy levels are denoted by |1⟩, |2⟩, |3⟩ and |4⟩ as shown in Fig. 1a. At the magnetic field strength of 500 G, the spin state of the NV center is effectively polarized to |mS = 0, mI = +1⟩ when a 532 nm laser pulse is applied.

Arbitrary single-qubit gates combined with applications of a maximally entangling two-qubit gate are sufficient for realization of universal two-qubit unitary operation. Our choice of a universal gate library consists of single-qubit gates and an entangling two-qubit gate, $U_{zz} = \exp(\imath mS_z \otimes I_z)$, which can be realized by the free evolution under the hyperfine coupling between electron spin and nuclear spin. We decompose a given two-qubit unitary operation $U$ into $U = (C \otimes D) \cdot V \cdot (A \otimes B)$ as shown in Fig. 1b, where

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Two-qubit programmable quantum processor in NV center. 

Fig. 1 Two-qubit programmable quantum processor in NV center. a Schematic atomic structure and energy levels of the NV center. The experiments are implemented on the two-qubit system composed of four energy levels within the dashed box (i.e., $|m_s = 0, m_I = \pm 1\rangle$, $|m_s = 0, m_I = 0\rangle$, $|m_s = -1, m_I = \pm 1\rangle$, and $|m_s = -1, m_I = 0\rangle$) denoted by $|1\rangle$, $|2\rangle$, $|3\rangle$, and $|4\rangle$. b Circuit diagrams for arbitrary unitary transformations. The brackets highlight the decomposition of arbitrary two-qubit operation into $\text{CNOT} \times V \times (A \otimes B)$. $R(\theta, \phi)$ corresponds to a rotation angle $\theta$ around the axis in the $XY$ plane. $\phi$ denotes the angle between the axis and the $X$ axis. $R(\phi)$ represents a rotation angle $\phi$ around the $Z$ axis. The entangling two-qubit gate $U_{zz}$ is $\exp(i m_S m_I)$. c Realization of the single-qubit gates. The single-qubit rotations on the electron spin are realized by hard microwave pulses with fixed Rabi frequency of $\Omega_{MW} = 40$ MHz. The duration of the pulses corresponds to the rotation angle $\theta$. The single-qubit rotations on the nuclear spin are realized by decoherence-protected gates consisting of dynamical decoupling of the electron spin and nuclear spin during the time interval. The strength of the nuclear spin driving is determined by the rotation angle $\alpha$. The time $\tau$ corresponds to the interaction between electron spin and nuclear spin state for the large Rabi frequency comparing to the hyperfine coupling $A_{zz}$. The length of the MW pulse $\tau$ is determined by the rotation angle $\theta$ as shown in the upper panel in Fig. 1c. Since the states of the electron and nuclear spin evolve and decoher at very different rates, decoherence-protected gates are implemented to realize the single nuclear spin rotation as shown in the lower panel in Fig. 1c. The XY-4 sequence is applied on the electron spin to protect the electron's coherence. The states of nuclear spin are driven during the time between the decoupling pulses. A rotation of the nuclear spin, which is independent of the electron spin state, is constructed by choosing $\tau = 2\pi n/A_{zz}$ with integer $n$. Here we fixed $\tau = 2777.8$ ns with $n = 6$ and the strength of the radio-frequency (RF) pulses is set as $\Omega_{RF} = \theta/4\tau$. The rotation around the $Z$ axis $R_z(\phi)$ is realized by adding a phase to the drive field for all subsequent gates.

To exhibit the flexibility of the processor to generate unitary transformations, we first implement the Deutsch–Jozsa algorithm as an example. It has been employed in different systems to demonstrate the exponential speedup in distinguishing constant from balanced functions with respect to the corresponding classical algorithm. A function that has an $n$-bit input and a 1-bit output ($f(0, 1, 2, \ldots, 2^n - 1 \rightarrow 0, 1)$) is balanced when exactly half of the
inputs result in the output 0 and the other half in the output 1, while a constant function assumes a single value irrespective of the input. The constant function \( f(0) = f(1) = 0 \) and the balanced function \( f(0) = 0, f(1) = 1 \) are mapped onto the unitary operators \( U_1 \) with \( U_1 = I \) and \( U_2 = \text{CNOT} \) as shown in the quantum circuit in Fig. 2a, where the \( I \) denotes the identity and the CNOT is the controlled-NOT gate. A measurement of the populations, \( P = \{P_1, P_2, P_3, P_4\} \), of the final state determines if the function is constant or balanced. The populations, \( P_i \), of the final state are determined by performing a set of measurements with different pulse sequences to redistribute the population of the final state. Comparing to the direct measurement of the final state, \( \pi_n \) and \( \pi_n \) pulses on the electron and nuclear spin respectively are also applied on the final state to flip the populations within the two-qubit system. The population of each energy level can be achieved from the resulting photoluminescence of these states. The entire quantum circuit combined with the flipping pulses can be treated as a unitary operator. This unitary operator is decomposed into the universal quantum circuit as shown in Fig. 1b following the three steps discussed above. The corresponding 15 parameters are shown in Table 1. Different unitary operators are implemented using the universal quantum circuit with different sets of parameters. Measurement of output \( P = (1000) \) indicates a constant function, while \( P = (0010) \) indicates a balanced function. In Fig. 2b, c, we show the measured population of each spin level of the final state after the Deutsch-Josza algorithm. The red bars indicate the ideal result, while the green bar is the simulation result considering the decoherence of the electron spin and the imperfect polarization (see Supplementary Information Section 2). The experimental results (blue bars) are in good agreement with the simulated results. The average success probability is 0.88(2) for constant and 0.93(2) for balanced functions.

Now we show that another quantum algorithm, named Grover search algorithm, can be executed by our programmable quantum processor by just adjusting the 15 parameters. The Grover search algorithm provides an optimal method for finding the unique input value \( x \) of a function \( f(x) \) that gives \( f(x) = 1 \) and \( f(x) = 0 \) for all other values of \( x \). It has been demonstrated in various systems\(^{21-24}\) in the two-qubit version of this algorithm there are four input values, \( x \in \{00, 01, 10, 11\} \), resulting in four possible functions \( f_j(x) \), with \( i, j \in \{0, 1\} \). These functions are mapped onto the C-Phase gate \( cU_j \) that encodes \( f_j(x) \) in a quantum phase, \( cU_j|\tilde{x}\rangle = (-1)^{f_j(x)}|\tilde{x}\rangle \). The C-Phase gate \( cU_j \) is denoted by the oracle \( U_j \) as shown in the quantum circuit in Fig. 3a. The quantum circuits to realize the C-Phase gate \( cU_j \) are designed specifically to the four cases in the conventional implementation of the two-qubit version of Grover search algorithm. In our work, the algorithm is demonstrated by the universal quantum circuit. The unitary operator of the four possible quantum circuit is programmed into the four sets of parameters as shown in Table 2. A measurement of the populations, \( P = \{P_1, P_2, P_3, P_4\} \), of the final

### Table 1. The parameters of the two-qubit programmable processor for Deutsch-Josza algorithm

| \( U_1 \) | \( U_2 \) | \( P_1 \) | \( P_2 \) | \( P_3 \) | \( P_4 \) |
|---|---|---|---|---|---|
| \( l \) | \( l \) | \( n/2 \) | \( n/2 \) | \( n/2 \) | \( n/2 \) |
| \( n_0 \) | \( n_1 \) | \( n_2 \) | \( n_3 \) | \( n_4 \) | \( n_5 \) |

The constant function and the balanced function are mapped onto the unitary operators

\[
U_{\text{const}} = \begin{cases} 
I & \text{for constant function,} \\
\text{CNOT} & \text{for balanced function.}
\end{cases}
\]

The experimental results of Deutsch-Josza algorithm with constant and balanced functions, respectively. The red bars are the ideal case. The green bars are the simulation results considering the imperfect polarization and the decoherence. The blue bars are the experimental results.
Experimental demonstration of Grover search algorithm. a Quantum circuit of Grover search algorithm. Four possible function $f_i(x)$ are mapped onto the oracle $U$, which is the C-Phase gate $cU_{ij}$. b–e The results of Grover search algorithm characterized by the population of each spin level of the final state. $P_1$, $P_2$, $P_3$, and $P_4$ denoted the population of $|1\rangle$, $|2\rangle$, $|3\rangle$, and $|4\rangle$, respectively. The red bars are the ideal case. The green bars are the simulated case considering the imperfect polarization and the decoherence. The blue bars are the experimental results.

Fig. 3 Experimental demonstration of Grover search algorithm. a Quantum circuit of Grover search algorithm. Four possible function $f_i(x)$ are mapped onto the oracle $U$, which is the C-Phase gate $cU_{ij}$. b–e The results of Grover search algorithm characterized by the population of each spin level of the final state. $P_1$, $P_2$, $P_3$, and $P_4$ denoted the population of $|1\rangle$, $|2\rangle$, $|3\rangle$, and $|4\rangle$, respectively. The red bars are the ideal case. The green bars are the simulated case considering the imperfect polarization and the decoherence. The blue bars are the experimental results.

Table 2. The parameters of the two-qubit programmable processor for Grover search algorithm

| $U_i$ | $U_{meas}$ | $\alpha$ | $\beta$ | $\delta$ | $\theta_A$ | $\phi_A$ | $\theta_{x,A}$ | $\phi_B$ | $\theta_{x,B}$ | $\theta_C$ | $\phi_C$ | $\theta_{x,C}$ | $\phi_D$ | $\theta_{x,D}$ |
|-------|------------|----------|----------|----------|-------------|-----------|-----------------|----------|-----------------|-------------|-----------|-----------------|----------|-----------------|
| $U_1$ | $I$        | 0        | 0        | 0        | $\pi/4$    | $\pi/2$   | 0               | $\pi/2$ | 0               | $3\pi/4$   | $\pi/4$   | $-\pi/2$        | $3\pi/2$ | $\pi/4$         | $-\pi/2$ | $\pi/2$         |
| $\pi_n$ | 0        | 0        | 0        | $\pi/4$ | $\pi/2$   | 0               | 0               | $3\pi/4$   | $\pi/4$ | $-\pi/2$        | $3\pi/2$   | $\pi/4$   | $-\pi/2$        | $3\pi/2$ | $\pi/4$         | $-\pi/2$ | $\pi/2$         |
| $\pi_n$ | 0        | 0        | 0        | $\pi/4$ | $\pi/2$   | 0               | $\pi/2$         | $3\pi/4$   | $\pi/4$ | $-\pi/2$        | $3\pi/2$   | $\pi/4$   | $-\pi/2$        | $3\pi/2$ | $\pi/4$         | $-\pi/2$ | $\pi/2$         |
| $U_2$ | $I$        | 0        | 0        | 0        | $\pi/4$    | $\pi/2$   | 0               | $\pi/2$ | $\pi$           | $3\pi/4$   | $\pi/4$   | $-\pi/2$        | $3\pi/2$ | $\pi/4$         | $-\pi/2$ | $\pi/2$         |
| $\pi_n$ | 0        | 0        | 0        | $\pi/4$ | $\pi/2$   | 0               | $\pi/2$         | $3\pi/4$   | $\pi/4$ | $-\pi/2$        | $3\pi/2$   | $\pi/4$   | $-\pi/2$        | $3\pi/2$ | $\pi/4$         | $-\pi/2$ | $\pi/2$         |
| $\pi_n$ | 0        | 0        | 0        | $\pi/4$ | $\pi/2$   | 0               | $\pi/2$         | $3\pi/4$   | $\pi/4$ | $-\pi/2$        | $3\pi/2$   | $\pi/4$   | $-\pi/2$        | $3\pi/2$ | $\pi/4$         | $-\pi/2$ | $\pi/2$         |
| $U_3$ | $I$        | 0        | 0        | 0        | $5\pi/4$   | $-\pi/2$ | $\pi$           | $\pi/2$ | 0               | $3\pi/4$   | $\pi/4$   | $-\pi/2$        | $3\pi/2$ | $\pi/4$         | $-\pi/2$ | $\pi/2$         |
| $\pi_n$ | 0        | 0        | 0        | $5\pi/4$ | $-\pi/2$ | $\pi$           | $\pi/2$         | $3\pi/4$   | $\pi/4$ | $-\pi/2$        | $3\pi/2$   | $\pi/4$   | $-\pi/2$        | $3\pi/2$ | $\pi/4$         | $-\pi/2$ | $\pi/2$         |
| $\pi_n$ | 0        | 0        | 0        | $5\pi/4$ | $-\pi/2$ | $\pi$           | $\pi/2$         | $3\pi/4$   | $\pi/4$ | $-\pi/2$        | $3\pi/2$   | $\pi/4$   | $-\pi/2$        | $3\pi/2$ | $\pi/4$         | $-\pi/2$ | $\pi/2$         |
| $U_4$ | $I$        | 0        | 0        | 0        | $5\pi/4$   | $-\pi/2$ | $\pi$           | $\pi/2$ | 0               | $3\pi/4$   | $\pi/4$   | $-\pi/2$        | $3\pi/2$ | $\pi/4$         | $-\pi/2$ | $\pi/2$         |
| $\pi_n$ | 0        | 0        | 0        | $5\pi/4$ | $-\pi/2$ | $\pi$           | $\pi/2$         | $3\pi/4$   | $\pi/4$ | $-\pi/2$        | $3\pi/2$   | $\pi/4$   | $-\pi/2$        | $3\pi/2$ | $\pi/4$         | $-\pi/2$ | $\pi/2$         |
| $\pi_n$ | 0        | 0        | 0        | $5\pi/4$ | $-\pi/2$ | $\pi$           | $\pi/2$         | $3\pi/4$   | $\pi/4$ | $-\pi/2$        | $3\pi/2$   | $\pi/4$   | $-\pi/2$        | $3\pi/2$ | $\pi/4$         | $-\pi/2$ | $\pi/2$         |

Four possible functions $f_i(x)$ are mapped onto the oracle $U$. The operation $U_{meas}$ indicates the measurement pulse after the algorithm, where $I$ denotes the identity and $\pi_n$ denotes single-qubit $\pi$ pulse on electron (nuclear) spin.

**DISCUSSION**

The algorithms presented here illustrate the computational flexibility provided by the solid-state spin-based quantum architecture at room temperature. The programmable quantum processor is capable of implementing arbitrary unitary operation on two qubits using the universal quantum circuit with altering state finds the state that has been marked. In Fig. 3b–e, we show the measured population of each spin level of the final state after the Grover search algorithm of four possible oracle functions. The experimental results (blue bars) are in good agreement with the simulated results (green bars). The average success probability is 0.85(1), 0.82(2), 0.81(2), and 0.84(2) for four possible functions, respectively.
the parameters. Substantial improvements could be made in the performance of the processor by using isotopically purified $^{12}$C, which would increase the coherence times of the qubits. Furthermore, dipolar coupling of electronic spins could mediate interactions between nuclear spins associated with different NV centers, offering a potentially scalable platform for information processing. Optical channels provide an alternate platform that is well suited to mediating interactions over macroscopic distances or in highly connected networks. With these improvements quantum computers with multiple qubits and fidelities above the fault-tolerance threshold should be realizable.

METHODS

Experiment setup

Our experiment was performed on a [100] oriented NV center in bulk diamond with low concentration of nitrogen impurity (<5 ppb) and natural abundance of $^{13}$C isotope (1.1%). The sample was mounted on a home-built confocal setup (see Supplementary Information Section 1 for the schematic of the setup). Optical excitation was provided by a 532 nm green laser, which was gated by an acousto-optic modulator. The laser beam was double passed through the acousto-optic modulator to suppress the laser leakage. And then the laser was delivered through an oil objective. The red fluorescence from the NV center was collected by an avalanche photodiode. A solid immersion lens was utilized to enhance the photon detection efficiency. The magnetic field was aligned along the NV symmetry axis ([1 1 1] crystal axis) by a permanent magnet. At the static magnetic field of 500 G, the state of the two-qubit solid-state quantum processor can be effectively polarized to $|m_z = 0, m_z = -1\rangle$ with 532 nm laser pumping. After the optical pumping, 95% of the population occupied the $|m_z = 0\rangle$ state of the electron spin and 98% of the population occupied the $|m_z = -1\rangle$ state of the nuclear spin. The microwave and radio-frequency pulses were created by an arbitrary waveform generator. Power amplifiers were utilized to amplify the pulses. A broadband coplanar waveguide with 15 GHz bandwidth was installed for the microwave pulses on the NV center. The radio-frequency pulses were carried by a home-built coil.

Code availability

The codes that were used in this study are available from the corresponding author upon reasonable request.

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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AUTHOR CONTRIBUTIONS

J.D. proposed the idea. J.D. and X.R. designed and supervised the experiments. Y.Wu, Y.Wu, X.R, and J.D. performed the experiments. Y.Wu, Y.Wu, X.R., and J.D. wrote the paper. All authors analyzed the data, discussed the results, and commented on the manuscript.

ADDITIONAL INFORMATION

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