Measurement of the atom number distribution in an optical tweezer using single photon counting

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We demonstrate in this paper a method to reconstruct the atom number distribution of a cloud containing a few tens of cold atoms. The atoms are first loaded from a magneto-optical trap into a microscopic optical dipole trap and then released in a resonant light probe where they undergo a Brownian motion and scatter photons. We count the number of photon events detected on an image intensifier. Using the response of our detection system to a single atom as a calibration, we extract the atom number distribution when the trap is loaded with more than one atom. The atom number distribution is found to be compatible with a Poisson distribution.

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I. INTRODUCTION

The last few years have seen a growing interest in the study of mesoscopic systems consisting of typically a few tens of interacting particles. The properties of these systems usually cannot be described by a mean-field approach and are already too complicated to be calculated from the behavior of each individual interacting particle. Dense clouds of ultra-cold atoms provide an ideal test bed to study these mesoscopic systems. The interactions are well-understood at the two-body level and, experimentally, one benefits from the host of tools developed over the years to investigate ultra-cold atomic clouds (see e.g. [1]). Various implementations have already been realized such as arrays of optical tweezers [2] or of magnetic traps [3], double-well potential geometries [4] and optical lattices (e.g. [5, 6]).

Beyond their intrinsic interest, a possible application of dense clouds of ultra-cold atoms is the production of atomic states for which the fluctuations of the number of atoms are reduced with respect to the Poissonian case. These clouds could for example be useful for atomic interferometry below the standard quantum limit [7]. Recent demonstrations have been achieved using Bose-Einstein condensates with a few thousand atoms ([8, 9]). The clouds could also be used as a source delivering a given number of atoms, as was already demonstrated in the single atom case in an optical tweezer [10] or in a one-dimensional optical lattice [11]. For larger numbers of atoms, experiments showing the reduction of the atom-number fluctuations have been reported in Bose-Einstein condensates in an optical trap [12], in optical lattices [13], or in arrays of magnetic micro-traps [14]. For all these applications the knowledge of the distribution of the number of atoms, and not only the average number of atoms, is essential.

The number of atoms in a cold atomic cloud can be measured by usual optical techniques, such as laser induced fluorescence or absorption. Nevertheless, special care must be taken when the number of interacting particles involved is small. For instance, when using fluorescence imaging the small number of atoms combined with the low collection efficiency makes it hard to collect more than a few photons per realization of the experiment, therefore preventing the reliable extraction of the number of atoms in single shot. To circumvent this problem, a method was recently demonstrated [15] where freely propagating atoms fall through a sheet of resonant light leading to the detection of many photons per atom.

In this paper we present a method to measure the distribution of the number of atoms trapped in a microscopic optical dipole trap in a regime where the number of atoms is a few tens. The method relies on single-photon counting. The principle is as follows: we release the cloud of cold atoms from the dipole trap and let them expand in a resonant light probe. The atoms diffuse in the probe in a Brownian motion and emit photons. Some of the photons are collected by an imaging system and impinge on an image intensifier where we count them. By repeating the experiment several times and recording the counting results, we reconstruct the distribution of the number of detected photons. Our experimental setup can work either with exactly one atom, or with a cloud of up to a few tens of atoms. In this way we perform a calibration of the number of detected photon events when a single atom is trapped, and use this calibration to determine the atom number distribution.

The paper is organized as follows. In Sect. II we describe briefly the setup. Section III describes the loading of our microscopic dipole trap in the single-atom regime and in the many-atom regime. In section IV we describe the experimental sequence and in Sect. V we present the image analysis used to count the number of photon events. Sect. VI deals with the calibration of our detection system using a single atom. Section VII explains how we extract the atom number distribution in the multi-atom regime. In Sect. VIII we compare the mean number of atoms extracted by this counting method to the

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result obtained by direct integration of the laser induced fluorescence, and find good agreement between the two methods.

II. EXPERIMENTAL SETUP

Our experimental setup has been described in details elsewhere [16–18] and consists essentially in a microscopic optical dipole trap, in which we trap up to a few tens of $^{87}$Rb atoms (see details in Section III). The trap is produced by a laser beam at 850 nm that is focused by an aspheric lens with a numerical aperture N.A. = 0.5. The resulting spot has a Gaussian profile with a waist $w = 1.1 \, \mu m$. A power of 9 mW yields a trap depth of 2 mK. The dipole trap is loaded from a cold atomic cloud held in a magneto-optical trap produced around the focal point of the aspheric lens. The magneto-optical trap captures atoms from a Zeeman decelerated atomic beam coming from an oven.

We use the same aspheric lens to collect the fluorescence light at 780 nm. A dichroic beam-splitter separates the fluorescence light from the dipole trap light. A fraction of the fluorescence light is sent to a fiber-coupled avalanche photodiode operating in a single photon counting mode. The remaining fluorescence is directed onto an image intensifier, followed by a low-noise CCD camera. We have measured a detection efficiency $\eta \approx 3 \times 10^{-3}$, which takes into account the solid angle of the aspheric lens (7%), the transmission of the optics (40%), and the measured quantum efficiency of the intensifier photocathode (10%). Here, we note that using an image intensifier is crucial for the experiment presented in this paper because it enables our imaging system to detect single photon events. In the absence of the intensifier, single photon events have an amplitude lower than the noise of the CCD camera alone ($6e^-/pixel$). The intensifier amplifies a single photon event to an average amplitude of $920e^-/pixel$, well above this noise level.

In order to characterize the atomic cloud, we use a probe consisting in two counter-propagating laser beams in a $\sigma_+ - \sigma_-$ configuration. This probe is tuned to the $(5^2S_{1/2}, F = 2)$ to $(5^2P_{3/2}, F' = 3)$ transition and is sent together with a repumping light tuned to the $(5^2S_{1/2}, F = 1)$ to $(5^2P_{3/2}, F' = 2)$ transition. The probe light is focused down to a waist of 0.9 mm and has a saturation parameter $I/I_{sat} \approx 2.7$ for each beam.

III. LOADING OF THE DIPOLE TRAP

The experiment can operate either in a regime where only one atom is present in the dipole trap or in a regime where up to $\sim 10$ atoms are trapped. The transition between the two regimes is governed by the atomic density in the magneto-optical trap, which is controlled by the flux of the atomic beam. The average number of atoms $N$ in the dipole trap is set by two competing processes: the loading from the magneto-optical trap, and the two-body losses due to collisions assisted by the near-resonant light of the cooling and trapping lasers [19]. When the loading rate of the dipole trap is lower than the light-assisted collision rate, only one atom can be present at a time in the trap: if a second atom enters the trap a light-assisted collision takes place and both atoms are lost. On the contrary, when the loading rate of the dipole trap overcomes the inelastic loss rate, the average number of atoms is larger than one [19, 20]. For the experiments presented below we find that, after a fixed loading time ($\lesssim 1$ s typically), the mean number of atoms in our microscopic trap increases linearly with the trap depth and reaches $N = 9$ for a trap depth of $\sim 20$ mK. We measure the temperature of the trapped atom(s) using either a release-and-recapture method [17] or a time-of-flight method [18]. We find a temperature around 150 $\mu$K in the single atom case and around 1 mK in the multi-atom regime.

In the single-atom regime, the presence of an atom in the trap is revealed by a step in the fluorescence signal collected on the APD [16]. This step is used to trigger an imaging sequence where the number of fluorescing atoms is exactly 1: this way there are no fluctuations in the atom number from shot to shot (variance $\Delta N^2 = 0$). In the multi-atom regime, the situation is different as we observe no such steps on the APD signal: firstly because when the atomic density increases, the time spent on average by each atom in the trap decreases below the time bin resolution of the APD counter due to an increasing inelastic loss rate, and secondly because the height of the steps itself decreases due to light-induced dipole-dipole interactions that shift and broaden the atomic line [21].

One thus cannot rely on fluorescence steps to perform an in situ measurement of the number of trapped atoms. Instead, the technique presented in this paper goes around this problem by converting the multi-atom signal into a sum of single atom events, spatially separated on a CCD camera. In this second regime, the absence of fluorescence steps on the APD signal also makes it impossible to trigger the imaging sequence after a given number of atoms is loaded in the trap. We thus trigger the imaging sequence after a fixed loading duration. Due to the random nature of the two-body losses during the loading this procedure leads to fluctuations in the number of trapped atoms from shot to shot ($\Delta N^2 \neq 0$) [19].

IV. EXPERIMENTAL PROCEDURE AND FLUORESCENCE IMAGES

Once the trap is loaded, either with exactly one atom, or with $N$ atoms, we switch off the cooling and repumping lasers and wait an additional 30 ms before switching off the dipole trap. This waiting period allows enough time for the atoms of the magneto-optical trap to leave the observation region, otherwise they would strongly contribute to the signal observed with the intensifier. We
then switch off the dipole trap (in ~ 200 ns) and, after a time of flight of the atoms of 1 µs in free space, we turn on the resonant probe, while gating the intensifier for a given period of time ∆t (in the 10–60 µsec range). Finally, we read out the CCD camera, which lasts ~ 500 ms, while launching the next loading sequence.

During the 1 µs time of flight in free space, the atoms start separating from each other. Then they walk randomly in the retro-reflected light probe and scatter photons at a rate ~ Γ/2 ≈ 2 × 107 s⁻¹ (Γ is the line-width of the atomic transition). Some of the scattered photons are collected on the image intensifier and impinge on the CCD at different positions due to the random walk of the atom in the probe light [22]. The total number n of detected events is proportional to the number of atoms N on average.

The images shown in Fig. 1(a) and (b) were obtained after a single realization of the experimental sequence. Figure 1(a) corresponds to the time of flight of a single atom moving randomly in the probe light. Figure 1(b) corresponds to the time of flight of about 8 initially trapped atoms. In both cases, the detected photons correspond in a large extent to photons being scattered by the atom and detected by the intensifier and, in a smaller extent, to photons due to spurious laser light or self-induced charges generated inside the intensifier (see more details below). This fact led us to adjust the size of the region of interest to the measured temperature of the atom(s): for a time of flight of duration ∆t, we chose a square with a side dimension ~ 4σᵥ∆t, where σᵥ = √kB T/M, T being the temperature of the atoms, M their mass, and k₅ the Boltzmann constant. This choice leads to a negligible probability of missing an atomic event, while reducing the number of background events, which are uniformly distributed on the CCD.

V. PROCEDURE FOR ANALYZING THE IMAGES

In order to count the number of events detected on the CCD camera, one has to decide what one calls an event. In order to do so, we first characterize the noise of the CCD camera, which is essentially due to the readout of the CCD chip. We find a root-mean-square (rms) noise σ CCD = 6e⁻/pixel. We then apply the following procedure. We search for the pixel with the largest amplitude of the signal. If the signal amplitude on this pixel is larger than 6σ CCD, we call it a peak and exclude from the image a zone of 13 × 13 pixels around it, the rms size of an individual event being 1.3 × 1.3 pixels (set by the intensifier resolution and corresponding to 0.6 × 0.6 µm² in the plane of the atoms) [22]. We then repeat this procedure by searching for the pixel with the next largest amplitude until no peak with an amplitude larger than 6σ CCD is found.

We have independently measured the amplitude distribution of single-photon events recorded by the intensifier followed by the CCD camera. Using this distribution, we have found that less than 4% of the events have a peak amplitude smaller than 6σ CCD. Our procedure for counting the events therefore does not underestimate their number by more than 4%.

VI. CALIBRATION USING A SINGLE ATOM

The first step of the calibration of the imaging system as a counting device was to measure the histogram of the number of background events in one image when no atom is trapped in the dipole trap. The background events have three different origins: the largest contribution comes from light scattering by the atoms of the atomic beam that cross the region of observation (60%); the second largest contribution comes from self-induced events generated by the gated intensifier when the high voltage is switched on and off (33% of the counts); finally, a smaller contribution comes from scattering of the probe beams on the surfaces inside the vacuum chamber (7%). The histogram of the total number of background events is shown in Fig. 2 which results from the analysis of 200 images of the background. The probe pulse duration was ∆t = 30 µs. The data are well fitted by a Poisson distribution with average 〈n bg 〉 = 0.7.

In a second step, we repeated the same experiment with exactly one atom trapped in the dipole trap. In particular, the probe duration was the same as above (Δt = 30 µs). As the detection efficiency is small and corresponds to a random collection of photons, we also expect a Poisson distribution for the number of detected photons emitted by the atom. In this case, the distribution of detected events, including the background events, is a Poisson distribution with a mean value:

\[ 〈n_{\text{single}}〉 = 〈n_{\text{at}}〉 + 〈n_{\text{bg}}〉 \]  (1)
served a linear dependency of the average number of detected events due to scattering by a single atom, shown in Fig. 3, where we plot the average number of detected photons, emitted by one atom, with the duration of the probe pulse. The results are calculated by analyzing 200 images. The error bar on each data point is obtained after subtraction of the average number of background events. We first performed the experiment with the duration of the atom illumination by the probe light. Linear fits to the data (dashed lines) yield a photon detection rate of $R_d = 57200 \pm 3100 \text{ s}^{-1}$ for 16 $\mu$K and $R_d = 61800 \pm 2400 \text{ s}^{-1}$ for 150 $\mu$K.

To conclude, we detect on average $\bar{n}_{\text{at}} = 1.1$ photons scattered by a single atom for a probe duration $\Delta t = 20 \mu s$. This value will serve as a calibration in the experiments described below, where the average number of atoms is the unknown.

VII. ATOM NUMBER DISTRIBUTION IN THE MULTI-ATOM REGIME

We now operate in the regime where more than one atom are loaded in the dipole trap. We repeat the same experimental procedure and extract the histogram of the number of detected events for a probe duration $\Delta t = 20 \mu s$. Figure 4 shows the histogram of the background events as well as the probability distribution of the total number of detected events (including the background events) when about 6.3 atoms are loaded in the dipole trap on average. The background gives an average number of events $\bar{n}_{bg} = 2.1$, larger than in Sect. VII as we needed to increase the flux of the atomic beam in order to load more than one atom in the trap.

To fit the distribution of events in the multi-atom regime, we consider the distribution of the number of atoms $N$ in the dipole trap, $P(N, \bar{N})$, with $\bar{N}$ the mean atom number. The probability to detect $n$ photon events is then given by the composed law 19:

$$p(n) = \sum_{\bar{N}=0}^{\infty} P(N, \bar{N}) \times \Pi(n, N \times \bar{n}_{\text{at}} + \bar{n}_{bg}) \quad (2)$$

with $\Pi(n, \alpha)$ the Poisson distribution of mean $\alpha$. Even in
Fig. 4 yields $\bar{n}$.

A direct calculation of the mean of the data shown in Fig. 4 is $\bar{n}_\text{at} = 1.1$. The data in red diamonds correspond to the background events only ($n_\text{bg} = 2.1$) fitted by a Poisson law. The duration of the probe is set to 20 $\mu$s so that the average number of detected photons scattered per atom is $\bar{n}_\text{at} = 1.1$.

The case when $P(N, \bar{N})$ is a Poisson law, the distribution $p(n)$ is not Poissonian. Nevertheless, for any distribution $P(N, \bar{N})$, the mean value of this composed law is given by:

$$\bar{n}_\text{multi} = \bar{N} \times \bar{n}_\text{at} + n_\text{bg}.$$  \hspace{1cm} (3)

A direct calculation of the mean of the data shown in Fig. 4 yields $\bar{n}_\text{multi} = 9$. Taking into account that the probe duration has been chosen to detect $\bar{n}_\text{at} = 1.1$ events per atom and that $n_\text{bg} = 2.1$, equation (3) yields an average number of atoms $\bar{N} = 6.3$. Taking a Poisson distribution for $P(N, \bar{N})$, a fit of the data by the composed law (2) leads to the same result. The result of the fit is shown in Fig. 4.

We now discuss the Poissonian assumption mentioned above for the atom number distribution $P(N, \bar{N})$. We extract from the data the variance of the number of detected events, $\Delta n^2_\text{multi} = n^2_\text{multi} - \bar{n}^2_\text{multi}$. This variance is related to the variance of the number of atoms $\Delta N^2$ by the following expression, calculated using the probability $p(n)$ of equation (2), and valid for any distribution $P(N, \bar{N})$:

$$\Delta n^2_\text{multi} = \bar{n}^2_\text{at} \times \Delta N^2 + \Delta n^2_\text{multi}.$$  \hspace{1cm} (4)

Taking again $\bar{n}_\text{at} = 1.1$, we find for the data of Fig. 4 a ratio of $\Delta N^2/\bar{N} = 0.86 \pm 0.13$ (the error bar is statistical). This value is compatible with $P(N, \bar{N})$ being a Poisson distribution. We repeat this measurement for various average numbers of atoms ranging from $\bar{N} = 2$ to $\bar{N} = 9$ and find that $\Delta N^2/\bar{N}$ is equal to 0.76 in average with a rms dispersion of 0.13. This 1 $\sigma$ uncertainty does not clearly indicate a sub-Poissonian behavior as $\Delta N^2/\bar{N}$ does not deviate from 1 by more than 2 $\sigma$.

VIII. COMPARISON WITH FLUORESCENCE INTEGRATION

We have checked that the average number of atoms extracted by the counting method described so far is consistent with the number of atoms extracted by a second method based on fluorescence integration. This second method consists in illuminating the cloud of freely propagating atoms by a 2 $\mu$s probe pulse, and accumulating the fluorescence detected on the CCD over many realizations of the experiment. In each time-of-flight experiment, we let the atoms fly during 1 $\mu$s before we illuminate them with the probe pulse. As explained in [12], after typically several hundreds repetitions of the experiment, the image shows a nearly gaussian distribution, reconstructed from many individual detected events. We perform this experiment in the multi-atom regime and then in the single-atom regime. We use the latter to extract the number of atoms in the multi-atom regime, by calculating the ratio of the integrated fluorescence values obtained in the two regimes.

This fluorescence integration based method was implemented in two trap configurations that we now describe. As already explained, a significant fraction of the background events come from photons being scattered when the atomic beam interacts with the probe light. To min-
imize this effect, we decreased the flux of the beam by reducing the temperature of the oven. This is at the expense of the loading rate of the dipole trap: in this first configuration, we could not load more than ~ 10 atoms in the microscopic dipole trap. In order to calibrate our detection scheme with a larger number of atoms, we implemented a dipole trap with a larger waist $w = 4 \mu m$. In this second configuration, the atomic density is smaller and the light-assisted collisions limit the number of atoms to a larger value than in the microscopic dipole trap \cite{20}, typically 30. The results of the experiment are shown in Fig. 5 where we plot the average number of atoms obtained from the counting method versus the average number of atoms obtained by fluorescence integration. The numbers of atoms obtained by the two methods are compatible: a linear fit to the data yields a slope of 1.08 which is compatible with 1, as the statistical uncertainty on the slope is 0.05 and we evaluate the bias uncertainties attached to each method to 4% for the counting method, and 11% for the integrated-fluorescence based method.

**IX. CONCLUSION**

We have demonstrated in this paper a method to reconstruct the distribution of the number of atoms trapped in an optical dipole trap. This method gives access to the distribution of the number of atoms for clouds containing up to a few tens of ultra-cold atoms. It is based on the detection, at the single photon level, of fluorescence events scattered by the atoms when they undergo a random walk in the resonant probe light. So far, we have investigated a regime where the distribution of the number of atoms does not clearly depart from a Poisson law. Our technique is in principle applicable to any distribution and could therefore be useful to investigate blockade effects leading to sub-Poissonian distributions of the number of trapped atoms.

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[22] The detected photon events are distributed around the geometrical images of the atoms according to the point spread function of the imaging system, which includes diffraction, residual aberrations and defocus due to the spatial distribution of the atoms. Given the size of the tweezers and the temperature of the atoms, the aberrations and the defocus are negligible. The collection efficiency therefore does not depend on the position of the atoms.
[23] The exclusion process may lead to missing neighboring peaks in the $13 \times 13$ pixels zone around the main peak. We have therefore developed a specific routine to treat these occurrences, which represent ~ 10% of the cases.