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Measurement of the Cosmic Microwave Background Polarization Lensing Power Spectrum from Two Years of POLARBEAR Data

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Abstract

We present a measurement of the gravitational lensing deflection power spectrum reconstructed with two seasons of cosmic microwave background polarization data from the POLARBEAR experiment. Observations were taken at 150 GHz from 2012 to 2014 and surveyed three patches of sky totaling 30 square degrees. We test the consistency of the lensing spectrum with a cold dark matter cosmology and reject the no-lensing hypothesis at a confidence level of $A_L = 1.33 \pm 0.32$ (statistical) $\pm 0.02$ (systematic) $\pm 0.07$ (foreground) using all polarization lensing estimators, which corresponds to a 24% accurate measurement of the lensing amplitude. Compared to the analysis of the first-year data, we have improved the breadth of both the suite of null tests and the error terms included in the estimation of systematic contamination.

Unified Astronomy Thesaurus concepts: Cosmic microwave background radiation (322); Gravitational lensing (670); Cosmology (343)

1. Introduction

The polarization of the cosmic microwave background (CMB) not only gives us insight into the earliest stages in the evolution of the universe, it also allows us to probe the large scale structure (LSS) formed more recently in cosmological history. CMB polarization can be separated into even parity $E$-modes and odd parity $B$-modes, and while the $E$-modes can be sourced from the same scalar perturbations that dominate CMB temperature anisotropies, $B$-modes are not generated through this mechanism to first order in perturbations.

Much effort is being devoted to using CMB $B$-modes for signs of primordial gravitational waves, but another expected source of $B$-modes is the gravitational lensing of the CMB by LSS (Lewis & Challinor 2006). This signature appears in the $B$-mode power spectrum as a signal peaking at an angular scale...
\( \ell \sim 1000 \). By mapping the CMB polarization, we can extract information about the distribution of LSS through reconstruction of the CMB lensing potential.

The CMB lensing potential is a representation of the matter power spectrum, integrated along the line of sight of CMB photons, which can tell us how much a given photon will be gravitationally deflected. For a gravitational potential \( \Psi \) we can integrate along the line of sight to calculate the lensing potential \( \phi \) (Hu & Okamoto 2002),

\[
\phi(n) = -2 \int_0^{\chi_s} d\chi \frac{\chi - \chi_s}{\chi} \Psi(\chi n, \chi),
\]

where \( \chi \) is the comoving distance and \( \chi_s \) is the comoving distance to the surface of last scattering. The lensing potential is related to the deflection field \( d = \nabla \phi \), which tells us how much a photon of the CMB is gravitationally deflected across the sky as it travels from the surface of last scattering to our detector.

We are able to reconstruct the lensing potential by taking advantage of the statistical properties of the CMB. At the surface of last scattering, the CMB is well described as a statistically isotropic Gaussian random surface of last scattering, the CMB is well described as a Gaussian random field, but gravitational lensing introduces non-Gaussianities that correlate CMB modes of different angular scale. This non-Gaussianity allows us to reconstruct the underlying lensing potential \( \phi \) by correlating \( E \)- and \( B \)-modes at varying angular scale (Hu & Okamoto 2002).

The science of CMB lensing contains a wealth of information about the more recent evolution of the universe, including the formation of LSS and the physics of neutrinos (Smith et al. 2009). The polarized CMB in particular is promising as a tracer of LSS because \( B \)-modes are not dominated by cosmic variance of the primordial CMB in the same way that the temperature and \( E \)-modes are at the present time. Additionally, polarization measurements are also less affected by many of the sources of contamination for the CMB temperature anisotropies, e.g., from the atmosphere or extragalactic foregrounds like the CIB and SZ-effects (Osborne et al. 2013).

The lensing potential has been detected using both CMB temperature and polarization fluctuations by a number of experiments including POLARBEAR—from the first season data set (Polarbear Collaboration 2014b), BICEP2/Keck Array (Ade et al. 2016), ACTPOL (Sherwin et al. 2017), Planck (Planck Collaboration VIII 2018), and SPTPOL (Wu et al. 2019).

Additionally, cross correlations between the CMB lensing potential with external tracers have been carried out in other works. These are valuable for combining information from two independent tracers of LSS while avoiding instrument-specific systematic errors (Bianchini et al. 2015).

Cross correlation with cosmic shear has been demonstrated by a number of experiments (Hand et al. 2015; Dark Energy Survey Collaboration et al. 2016; Kirk et al. 2016; Liu et al. 2016; Hildebrandt et al. 2017; Singh et al. 2017; Omori et al. 2019), deriving results primarily from CMB temperature. The data set of this paper has also been used in a cosmic shear cross correlation with Subaru Hyper Suprime-Cam (Namikawa et al. 2019). Cross correlation with the cosmic infrared background have been conducted as well (Holder et al. 2013; Planck Collaboration et al. 2014; Polarbear Collaboration 2014a; van Engelen et al. 2015; Planck Collaboration VIII 2018).

Additionally, this data set has been cross correlated with submillimeter galaxy counts from the Herschel-ATLAS (Polarbear Collaboration 2019) experiment.

The search for CMB \( B \)-modes from gravitational waves can be improved if the \( B \)-mode signal from gravitational lensing is reduced. This “delensing” has been done using several methods. External tracers of the lensing potential have been combined with CMB observations (Sherwin & Schmittfull 2015; Manzotti et al. 2017) to subtract templates of gravitational lensing and reduce the final \( B \)-mode power. Internal delensing has also been achieved in which the lensing potential and \( B \)-modes are constructed using the same data set (Carron et al. 2017), and in another work we demonstrate internal delensing of the CMB using only polarization data (Polarbear Collaboration 2020). Both of these delensing methods are useful, but of the two, internal delensing has been forecast to achieve the best performance for sufficiently low noise measurements (Carron 2019).

In this work we show a reconstruction of the lensing potential power spectrum from observations by the POLARBEAR experiment. We have observed an area of \( \sim 30 \) square degrees with one of the lowest levels of arcminute scale noise yet achieved. The lensing information is dominated by polarization rather than temperature anisotropies. This deep data set has enabled a polarization-only reconstruction of the lensing potential power spectrum, and has served as a useful data set for additional cross correlation and delensing studies.

### 2. Lensing Power Spectrum Analysis

The polarization-sensitive POLARBEAR experiment is located at the James Ax Observatory in Northern Chile on Cerro Toco. It uses 1274 transition-edge sensor bolometers to observe the CMB at 150 GHz and has a 2.5 m primary mirror that produces a beam with a 3.5′ full width at half maximum (FWHM).

We observe three sky patches over a time period of two years from 2012 to 2014, each with an extent of approximately \( 3^\circ \times 3^\circ \). They are centered in right ascension and declination at \( (4^h 40^m 12^s, -45^\circ 00^\prime) \), \( (11^h 53^m 00^s, -0^\circ 30^\prime) \), and \( (23^h 48^m, -32^\circ 48^\prime) \) which we will refer to with the respective names RA4.5, RA12, and RA23. More details on the receiver and telescope can be found in Arnold et al. (2012) and Kernish et al. (2012). One advantage of observing small patches is the ability to obtain deeper observations over a given amount of time. The polarization white noise levels for RA4.5, RA12, and RA23 respectively are 7, 6, and 5 \( \mu \)K arcmin. After accounting for beam and filter transfer functions, the effective polarization noise levels (defined as the minima of the resulting \( N_L \) noise curves) are 10 \( \mu \)K arcmin, 7 \( \mu \)K arcmin, and 6 \( \mu \)K arcmin, respectively.

This analysis builds on previous results from the POLARBEAR collaboration using the same data set described above. We have shown evidence of \( B \)-mode power induced by gravitational lensing (Polarbear Collaboration 2017), which we will refer to as PB17. The CMB maps used in that analysis are also used here.

We also showed evidence of the lensing potential auto-power spectrum itself in a previous work (Polarbear Collaboration 2014b) that used only our first season of observations. We will refer to that paper as PB14. This paper improves upon that work by adding a second year of observations.
observations on the same set of three patches, which corresponds to an increase in data volume of 61% over PB14. We also note that in PB14, we used a separate analysis pipeline from our B-mode analysis to generate simulations and perform null tests. This time our analysis uses the same pipeline to generate lensed and filtered CMB simulations as used in PB17, so that the details of our mapmaking and instrumental systematic estimation are consistent across both publications. This has the advantage that our simulations now accurately model our mapmaking procedure starting at the timestream level and include the anisotropic effects of our timestream filters in the lensing reconstruction step. Additionally we have included a set of data split null tests not present in our first season lensing analysis, these are described in more detail in Section 3.1.

In our data analysis pipeline, we start with Q and U CMB maps to obtain weighted E- and B-modes using the data model

\[ d_i = P_{ik} s_k + n_i, \]  

where \( d_i \) contains the pixelized real space Q and U maps, \( n_i \) are the pixelized map domain noise contributions, and \( s_k \) are the E- and B-mode fields. \( P_{ik} \) is the matrix operator that encodes effects from the beam and timestream filtering, and transforms from Fourier space to real space. The index \( i \) includes Q/U and pixel indices \( i = (M, p) \), and the index \( k \) includes E/B and mode indices \( k = (\ell, \ell') \).

We obtain inverse-variance Wiener-filtered CMB E- and B-modes, \( \tilde{X}(\ell) \), from the observed Q and U maps, \( d \), using the matrix equation

\[ \tilde{X} = S^{-1}[S^{-1} + P^{-1}N^{-1}]^{-1}P^{-1}N^{-1}d, \]  

where \( S_{kk} = \delta_{XX} \delta_{LL} \mathcal{C}_{XX} \) and \( N_{pp} = \delta_{MM} \delta_{pp} \mathcal{N}_M^{-1} \mathcal{N}_P^{-1} \). \( \mathcal{C}_{XX} \) are the fiducial CMB power spectra for \( X \in \{Q, U\} \) and \( N_M^{-1} \) is the noise map where \( p \) labels a given pixel in the map and \( M \in \{Q, U\} \). Our noise weighting also includes a cutoff for pixels with noise levels above 55 \( \mu \)K arcmin and point-source masking for sources above 25 mJy in intensity. The CMB power spectra used for this Wiener filter are generated using the freely available software package CAMB.28 and use the Planck 2015 best-fit cosmological parameters (Planck Collaboration XIII 2016),29 which is the same parameter set used in PB17.

From the inverse variance weighted modes \( \tilde{X}(\ell) \) we then reconstruct the lensing potential using the quadratic estimator

\[ \hat{\phi}^{XY}(L) = A(L) \int d^2\ell \tilde{X}(\ell) \tilde{Y}^\dagger(\ell - L) F_{XY}(\ell, \ell - L), \]  

where the normalization is defined by

\[ A^{-1}(L) = \int d^2\ell f_{XY}(\ell, \ell - L) F_{XY}(\ell, \ell - L), \]  

and the weights \( f_{XY}(\ell, \ell - L) \) and \( F_{XY}(\ell, \ell - L) \) are described in detail in Hu & Okamoto (2002).

In addition to our data we also use a set of 500 Monte Carlo (MC) simulations in our analysis to estimate the lensing mean field, noise bias, transfer function, and covariance matrix. We generate realizations of lensed CMB signal that are mock observed using the same pointing, noise level, and scan strategy as our real observations. These timestreams are then run through our mapmaking pipeline and the resulting Q and U maps are used as inputs to our lensing pipeline as described in the above equations.

The process of going from quadratic estimates of the lensing potential \( \hat{\phi}^{XY}(L) \) to power spectra follows the method we used in PB14. First, we estimate the mean field from our set of MC simulations and subtract that from \( \hat{\phi}^{XY}(L) \). Next, we correlate two reconstructed lensing maps \( \phi_{UV}^{XY}(L) \) and \( \phi_{XY}^{XY}(L) \) to construct the pseudospectra \( \tilde{C}_{L}^{XY} \), where the indices UV, XY indicate the type of estimator (EE or EB). We follow Hanson et al. (2011) and Namikawa et al. (2013) to estimate the realization-dependent noise bias \( N_{L}^{(0),UVXY} \) using lensing reconstructions of our data and MC simulations. Once bias subtracted spectra from simulations are constructed, we then estimate the transfer function by taking the ratio between the mean of these reconstructed lensing power spectra and the input theory power spectra used to generate them. And, finally, this transfer function is used to correct the lensing potential power spectrum estimate of our data giving us our final spectra as defined by the equation,

\[ C_{L}^{UVXY} = (\tilde{C}_{L}^{XY} - N_{L}^{(0),UVXY})/T_L. \]  

Here, \( T_L \) is the transfer function that corrects for the effects of filtering and weighting in our pipeline and \( C_L \) is the lensing potential power spectrum. The lensing estimators are labeled here by UV, XY \( \in \{EE, EB\} \). Additionally, while we only used \( C_{L}^{EEE} \) and \( C_{L}^{EEB} \) in PB14, we include the power spectrum estimator \( C_{L}^{EEE} \) in this analysis.

We also considered including an estimate of the \( N^{(1)} \) bias but ultimately did not use it for this analysis because its expected size is small relative to our lensing spectrum sensitivity. We compared analytical estimates of this bias to the size of our statistical errors for each of the lensing estimators and found that the relative size of the \( N^{(1)} \) bias is only a few percent. Estimates of this bias were calculated with publicly available software.30 using numerical methods shared by other codes (Carron & Lewis 2017).

To estimate the amplitude of lensing, we use 500 MC simulations to construct the covariance between our three \( C_{L}^{XY} \) estimators. If we label the estimator \( \alpha = UVXY \in \{EEE, EEB, EEBEB\} \), and the covariance matrix \( C_{\alpha\alpha'} \) represents the covariance between the bandpower \( C_{\alpha} \) and \( C_{\alpha'} \), then the lensing amplitude is

\[ A_{\alpha} = \frac{\sum_{L,L'} C_{L}^{(th)} C_{\alpha}^{-1} C_{L,L'}^{-1} C_{\alpha'}^{(th)}}{\sum_{L,L'} C_{L}^{(th)} C_{\alpha}^{-1} C_{L,L'}^{(th)}}, \]  

and the inverse variance on the amplitude is given by

\[ (\sigma_{\alpha})^{-2} = \sum_{L,L'} C_{L}^{(th)} C_{\alpha}^{-1} C_{L,L'}^{(th)}, \]  

where the \( (th) \) superscript denotes the theory power spectrum.

Finally we have also found that our observations are polarization dominated. While we do not include temperature in the results presented here, we have compared \( N_{L}^{(0)} \) bias curves from temperature-only information (the TT estimator) and from polarization-only information (the EE and EB estimators) and found lower noise in polarization.

28 https://camb.info/
29 in the base_plikHM_TT_lowTEB_lensing configuration.
30 github.com/JulienPeloton/lensingbiases
First versus second seasons of data collection  
Close to Sun versus far from Sun  
Day versus night  
First half versus second half by data volume  
Rising versus setting  
High elevation versus low elevation  
High versus low detector gain  
Good versus bad weather  
Q versus U pixels  
Left versus right side of the focal plane  
Left versus right scan direction  
Close to moon versus far from moon

Note. The 12 ways that we split the data set for null tests that probe potential unmodeled systematic errors.

### Table 1

| Data Split Null Test Types |
|-----------------------------|
| Close to Sun versus far from Sun |
| Day versus night |
| First half versus second half by data volume |
| Rising versus setting |
| High elevation versus low elevation |
| High versus low detector gain |
| Good versus bad weather |
| Q versus U pixels |
| Left versus right side of the focal plane |
| Left versus right scan direction |
| Close to moon versus far from moon |

### 3. Null Tests

We perform a blind analysis and therefore need a way to guard against unknown systematics and validate our error-bar estimation, which we address through a set of null tests. We only examine our final power spectra after all of our null tests satisfy passing criteria that demonstrate our analysis is performing as expected.

All of the simulations used in the following null tests are generated at the timestream level. They use the same pointing reconstruction used for real observations to mock simulate CMB signal sky observations, and include noise at the timestream level based on a white noise model consistent with the real observations of the second season in PB17. The resulting simulated timestreams are run through the same mapmaking and lensing reconstruction pipelines as is used for the real data.

### 3.1. Data Split Null Tests

We perform one suite of null tests constructed from splits in our data selection. We choose 12 splits to probe potential systematic errors that are not captured by the lensing analysis pipeline. The splits are listed in Table 1. These are the same data splits used in PB17, where more detailed description of the 12 data splits can be found.

For each of these 12 data splits we construct two sets of lensing estimates, $\hat{\phi}_V^{UV}$ (L) and $\hat{\phi}_V^{XY}$ (L) for the first set of the split data set and $\hat{\phi}_V^{XY}$ (L) and $\hat{\phi}_V^{UV}$ (L) for the second set of the split data set. We then construct the auto spectra of each of the two sets and the cross spectra between the two sets, including a noise bias subtraction for each of these component spectra. Finally we use these to construct the null spectrum

$$C_L^{null} = C_L^{UVXY} + C_L^{UVXY} - C_L^{UVXY} - C_L^{UVXY}$$

We evaluate this set of 108 null spectra (from 12 splits, 3 power spectrum estimators, and 3 sky patches) similarly to the procedure used in PB17.

Using nine equally spaced bins $b$ in the multipole range $100 < \ell < 1900$ and an estimate of the standard deviation $\sigma_b$ from MC simulations we construct the quantity $\chi^2_{null}(b)$

$$\chi^2_{null}(b) \equiv \frac{C_b^{null} - \sigma_b}{\sigma_b}.$$  

For each patch, we then calculate the probability to exceed (PTE) value for five quantities: the average value of $\chi^2_{null}(b)$, the worst value of $\chi^2_{null}(b)$, the worst value of $\chi^2_{null}$ by spectrum (summed over all bins), the worst value of $\chi^2_{null}$ by test, and finally the total value of $\chi^2_{null}$ for each patch. The simulated data, which are generated from the simulated timestreams, are split the same way as the observed data. The error bars $\sigma_b$ are then estimated from an ensemble of 500 simulated data splits. The results from these null tests are summarized in Table 2.

Before unblinding our data we summarize the five tests just described by calculating a total PTE, labeled “All stats” in the rightmost column of Table 2. We require this value to be greater than 5%. To calculate this, we take the worst of the five $\chi^2$ PTEs from the data (in each row of Table 2) and compare it to the worst PTE from a distribution of simulations. The resulting “All stats” PTE is then the fraction of the simulations that exceed the data.

The worst $\chi^2$ PTEs are calculated in a similar manner. We calculate one value of $\chi^2_{data}$ from the data and 500 values of $\chi^2_{sim,i}$ from a distribution of MC simulations. The PTE value is then equal to the fraction of the simulations such that $\chi^2_{sim,i} > \chi^2_{data}$. The only exception to this rule is the average $\chi^2_{null}(b)$ PTE, which we evaluate by performing a two sided test. We calculate the average $\chi^2_{data}$ from data and the average $\chi^2_{sim,i}$ for each simulation and the corresponding PTE is equal to the fraction of the simulations such that $\chi^2_{sim,i} > \chi^2_{data}$.

### 3.2. Curl and Cross-patch Null Tests

Additionally we conduct a set of lensing specific null tests using the full data set. First we generate curl reconstructions of the lensing deflection field $\nabla \times \mathbf{d}(\hat{n})$, which we expect to be vanishingly small and serve as a check on unmodeled systematics (Cooray et al. 2005).

We also generate cross power spectra between lensing reconstructions from two different observational patches. These independent measurements should lack any common signal, so any significant deviation from a null spectrum would indicate a misestimation of our error bars or a spurious correlation introduced by our analysis pipeline.

Both of these tests were also performed in PB14. Our passing criteria for these sets of tests are similar to our criteria for the data split null tests. We calculate the worst $\chi^2$ PTEs corresponding to the average of $\chi^2_{null}(b)$, extreme of $\chi^2_{null}(b)$, extreme of $\chi^2_{null}$ by spectrum, and a total $\chi^2_{null}$, in addition to a combined PTE combining all four of those statistics. We consider the data set to have passed these tests if the final PTE accounting for all statistics is greater than 5%. The results from this set of null tests are summarized in Table 3, in particular, showing that the PTEs for all statistics are 53.0% for the curl tests and 60.2% for the cross-patch tests. We also note that these null tests do not require a noise bias subtraction and thus are not affected by the noise bias calculation subtlety described in the Appendix.

### 4. Contamination

We use a difference spectrum framework to evaluate the effect of instrumental systematic and foreground contamination to the lensing spectrum by looking at the effect on $A_L$.

Using a set of MC simulations, we calculate two lensing power spectra for each CMB realization. The first spectrum is created with the fiducial pipeline while the second spectrum is created by adding a realization of the contamination at map level to our $Q$ and $U$ maps. The difference between these two is
null test criteria. We also checked to see if the distribution of all PTEs agree with a uniform distribution via the Kolmogorov–Smirnov test and found that for all of our patches the null PTEs are indeed consistent with a uniform distribution as expected. One notable feature of the table is a preponderance of high PTE values, which is caused by our treatment of the noise bias subtraction. We elaborate on this in the Appendix but otherwise we find no evidence for systematic biases in the data.

used as our estimate of contamination,

$$\Delta C^c_L = C^c_L - C_L,$$

(10)

where $C^c_L$ denotes the lensing power spectrum calculated including contamination while $C_L$ is the spectrum calculated without contamination.

### 4.1. Instrumental Systematics

In PB17 we used simulations of systematic effects to estimate their contributions to the $C^{\text{BB}}_L$ power spectrum. This systems pipeline was incorporated into our main analysis pipeline and generated contamination at the timestream level that modeled a number of different instrumental systematic effects. We use that same systematic simulation pipeline here to estimate contributions to the lensing power spectrum.

For each instrumental systematic effect we use 100 MC estimates of $\Delta C^c_L$. The mean value of these spectra and their covariance are then used to calculate an effective lensing amplitude due to systematic contamination, $A^c_L \pm \sigma^c_L$. To evaluate any bias introduced to $A_L$ by a given systematic effect, we calculate an upper limit $\Delta A^c_L$ on the lensing amplitude given by

$$\Delta A^c_L = |A^c_L| + \frac{\sigma^c_L}{\sqrt{100}}.$$  

(11)

In addition to limits on systematic bias to the lensing power spectrum, we also account for the extra variance introduced by systematic effects through their effects on $\sigma_A$. We add in quadrature all the values of $\sigma_A$ in our final estimation of $A_L$.

A summary of the contributions $\sigma^c_A$ and $\Delta A^c_L$ from each systematic effect is shown in Table 5, in particular, showing that the total contribution to $\sigma_A$ is 0.02 and our upper limit on systematic bias from all modeled effects is 0.006.

### 4.2. Foregrounds

We use the Planck 2015 frequency maps to estimate the impact that foregrounds have on our reconstruction of gravitational lensing (Planck Collaboration IX 2016; Planck Collaboration X 2016). In particular, we use the Planck 30 GHz and 353 GHz all sky intensity maps as tracers of synchrotron and dust foreground power, respectively. Our observational patches were chosen, in part, because they have very low foreground power. Thus, the Planck polarization maps are dominated by noise in the regions of the sky that we observed. Therefore, to estimate a conservative upper limit on foreground power, we use a polarization fraction of $p = 20\%$ and constant polarization angle in combination with Planck intensity maps to generate maps of polarized foregrounds in our three patches.

This method does have certain drawbacks. The synchrotron estimate, in particular, has limited information of smaller scales due to the half degree beamwidth of the Planck 30 GHz observations. However, selecting for regions of very low foreground power means that an estimate from a method like simulations from a fitted foreground template would not be representative of these regions so we instead use direct observations as a tracer. Similarly, a constant polarization angle is only an approximation but since polarization angles are coherent across scales larger than our patch we use a constant angle as a close approximation in the absence of high quality measurements of the underlying angle distributions.

Additionally, the overall estimates of dust and synchrotron power in these patches are, respectively, three and five orders of magnitude smaller than the $E$-mode power which dominates the reconstructions and at least two orders of magnitude smaller than the noise power. Even if there were moderate errors in foreground estimation, we can sensibly say that the overall contributions to the lensing spectra would be negligible. And as a final check, the curl null tests previously described are sensitive to foreground power and the passing of these tests indicates that there is not a significant level of foreground contamination.

The amplitudes of these Planck maps are scaled to 150 GHz assuming a modified blackbody spectral dependence for thermal dust and a power law for synchrotron (Krachmalnicoff et al. 2018; Planck Collaboration XI 2018), and then simulated timestreams are produced and run through our analysis pipeline in order to include the scan strategy, time stream processing, filtering, and other effects that are incorporated in our real observations.

Finally, contributions to the lensing power spectrum $\Delta C^c_L$ for our dust and synchrotron estimates are constructed using the same method as the instrumental systematics, and contributions to the bias and uncertainty on $A_L$ are calculated and listed in Table 5.

### 5. Results

We present the minimum variance power spectrum in Figure 1, which combines power spectra from our three observational patches and the three polarized estimators. The bandpowers and error bars are listed in Table 6. The statistical uncertainty on our measurement of $A_L$ is calculated from the standard deviation of the distribution of simulated $A_L$ from 500 signal-plus-noise MC simulations. Including uncertainty from instrumental systematics and foreground contamination, our measurement of the lensing amplitude is $1.33 \pm 0.32$ (statistical) $\pm 0.02$ (systematic) $\pm 0.07$ (foreground), corresponding to a significance of 4.1$\sigma$.
Extreme of $\chi^2_{null}(b)$ and cross-patch null tests. Again we see that all of the individual worst $\chi^2_{null}$ criteria and the PTE combining all stats in the rightmost column are all above the required null test threshold. Like the data split tests, we also tested the distribution of PTEs and found they are consistent with a uniform distribution via the Kolmogorov-Smirnov test.

### Table 3

PTEs Resulting from the Curl and Cross-patch Null Tests

| Test   | Average of $\chi^2_{null}(b)$ | Extreme of $\chi^2_{null}(b)$ | Extreme of $\chi^2_{null}$ by Spectrum | Total $\chi^2_{null}$ | All Stats |
|--------|-----------------------------|--------------------------------|--------------------------------------|------------------------|-----------|
| curl   | 48.6%                       | 23.8%                          | 58.6%                                | 64.8%                  | 53.0%     |
| cross  | 95.4%                       | 16.0%                          | 27.4%                                | 16.2%                  | 60.2%     |

**Note.** PTEs resulting from the curl and cross-patch null tests. Again we see that all of the individual worst $\chi^2_{null}$ criteria and the PTE combining all stats in the rightmost column are all above the required null test threshold. Like the data split tests, we also tested the distribution of PTEs and found they are consistent with a uniform distribution via the Kolmogorov-Smirnov test.

### Table 4

Contributions to $A_L$ from Instrumental Systematic Effects

| Effect [×10$^3$] | $A_L'$ | $\sigma_{A_L}'$ | $\Delta A_L'$ |
|------------------|--------|-----------------|---------------|
| Crosstalk        | -0.28  | 1.9             | 0.47          |
| Pointing         | 3.60   | 21.2            | 5.72          |
| Beam Ellipticity | 0.54   | 1.5             | 0.69          |
| Beam Size        | 0.16   | 1.8             | 0.34          |
| Gain Drift       | 0.14   | 2.7             | 0.41          |
| Relative Gain    | -0.67  | 4.9             | 1.16          |
| Total            | 22.1   | 5.92            |               |

**Note.** All values have been multiplied by a factor of 10$^3$ for display in this table. The resulting total contribution to our uncertainty on the lensing amplitude is $\sigma_{A_L}' = 0.022$, and our upper limit on the total systematic bias is $\Delta A_L' = 0.006$.

### Table 5

Contributions to $A_L$ from Foreground Contamination

| Effect [×10$^3$] | $A_L'$ | $\sigma_{A_L}'$ | $\Delta A_L'$ |
|------------------|--------|-----------------|---------------|
| Dust             | 3.16   | 65.1            | 9.67          |
| Synchrotron      | -0.42  | 7.6             | 1.18          |
| Total            | 65.5   | 9.74            |               |

**Note.** All values have been multiplied by a factor of 10$^3$ for display in this table. The resulting total contribution to our uncertainty on the lensing amplitude is $\sigma_{A_L}' = 0.066$, and our upper limit on the total systematic bias is $\Delta A_L' = 0.0097$.

### Table 6

Minimum Variance Spectrum Bandpowers

| $L_{\text{min}}$ | $D_L [\times 10^{-8}]$ |
|------------------|------------------------|
| 200              | 10.47 ± 1.91           |
| 400              | 1.55 ± 1.38            |
| 600              | 1.96 ± 1.15            |
| 800              | 0.70 ± 1.14            |
| 1000             | -1.51 ± 1.33           |
| 1200             | -1.08 ± 1.67           |
| 1400             | -0.58 ± 2.41           |
| 1600             | -0.19 ± 3.35           |
| 1800             | 4.28 ± 4.13            |

**Note.** The minimum variance power spectrum $D_L = L(L + 1)C_L/2\pi$ with 1σ error bars, multiplied by a factor of 10$^8$ in this table for display purposes.

Additionally, we examine the no-lensing hypothesis using a set of 500 MC simulations that do not include gravitational lensing. The distribution of unlensed simulations has a width of $\sigma_A = 0.12$, corresponding to a forecasted significance of 8.3σ. The suboptimal weighting in the lensing estimator due to the assumption of no-lensing has the effect of shifting the value of the lensing amplitude. The power spectrum calculated under the no-lensing assumption on our data has an estimated amplitude of $A_L = 1.52$. The shift in $A_L$ from the lensed to unlensed case here is similar to the shift seen between the two $A_L$ values reported in PB14. Including uncertainty from systematics and foregrounds and our observed value of $A_L$, we reject the no-lensing hypothesis at a significance of 10.9σ, which is a considerable improvement upon the 4.2σ rejection from our earlier work in PB14. Distributions of the $A_L$ calculated from simulations in the lensed and unlensed cases are shown in Figure 2.

We evaluate the consistency of our three patches by comparing the patchwise minimum variance power spectra $C_L^{p}$, $p \in \{RA23, RA12, RA4.5\}$ between pairs of patches using PTEs of the quantities $C_L^{p} - C_L^{p'}$. Additionally, we note that the first bin in the power spectrum for RA12 is considerably higher than the other two so we also evaluate PTEs specifically comparing the values in the first bin of each of our three patches. The results of these tests are summarized in Table 7, and they confirm that the three patches are consistent with each other.

This modest excess of power in RA12 is also seen in cross-correlation analyses with Herschel-ATLAS and Subaru Hyper Suprime-Cam (Namikawa et al. 2019; Polarbear Collaboration 2019), both of which use independent analysis pipelines. In particular when looking at the Herschel-ATLAS galaxy auto-power spectra of RA23 and RA12 patches, we see that RA12 has a modest excess in power in the lowest multipole bin similar to what we see in the present analysis. This gives
We evaluate the consistency of our three patches with PTE values for the
Note.
RA4.5 versus RA23 89.2% 56.2%
RA12 versus RA4.5 49.6% 8.0%
RA23 versus RA12 24.8% 35.6%
simulations. In both cases, the blue histogram represents the distribution of
temperature and polarization CMB power spectra gives a value

delensing
which is summed over power spectra for all estimators and patches, nine in total. Relative to our best-fit value of
is 1.33 that we achieve from the POLARBEAR data set, we find a PTE of 58.8%, and relative to the value of
expected from ΛCDM we find a PTE of 5.0%, which indicate that our results agree with our current understanding of the

cosmological standard model.
We can also consider our result in light of recent results for
from Planck. The lensing smoothing effect on the Planck
temperature and polarization CMB power spectra gives a value of
1.180 ± 0.065 (Planck Collaboration VI 2018) which differs from
1 by 2.8σ, while the measurement from Planck lensing reconstruction (Planck Collaboration VIII 2018)
is consistent with ΛCDM with the value
1.011 ± 0.028. While our own value is also consistent with ΛCDM, we note that our estimate of
is consistent with both of these Planck estimates of the lensing amplitude.

6. Conclusion
We have presented a measurement of gravitational lensing of
the polarized CMB. This work was performed using a blind
analysis framework that subjected our data set to a suite of null
tests to validate error bars and show that our data selection and
analysis pipeline are not contaminated by unknown systematic errors. We include the impact of known foreground
and instrumental systematic errors in our final estimations, and we
reject the no-lensing hypothesis at a significance of 10.9σ. The
lensing power spectrum derived using a minimum variance estimator from the second season data is measured as
1.33 ± 0.32 (statistical) ±0.02 (systematic) ±0.07 (foreground), which is a 4.1σ measurement and is consistent with the current ΛCDM cosmology.

The lensing information in the POLARBEAR data presented here is derived from polarization information. Polarization
measurements of gravitational lensing will become increasingly
more relevant as more experiments are dominated by polarization rather than temperature information. This work
joints our other cross-correlation (Namikawa et al. 2019; Polarbear Collaboration 2019) and delensing (Polarbear
Collaboration 2020) analyses in exploring signals of gravitational
lensing present in CMB polarization.

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Appendix

Data Split Null Test PTE Values

As mentioned in Section 2, we estimate a realization-dependent noise bias as part of calculating the lensing spectrum for our data set. This step is computationally expensive and ideally we would estimate a realization-dependent bias for the data and each of the 500 MC simulations to ensure they are all treated exactly the same by our analysis pipeline. However, it was only computationally reasonable for us to estimate a realization-dependent bias for the data, and instead we use the easier to calculate Gaussian bias for each of our simulations.

A possible effect of using a slightly more accurate noise bias subtraction on the data than on the simulations is that we may get higher PTEs in our null tests than if we had used a realization-dependent bias for all simulations. In Table 2 it appears that such an effect might be resulting in high PTEs, considering the fact that out of 18 statistics the lowest PTE value is 35.8%. To determine if these high values are the result of the difference in bias calculation between data and simulations, we perform an additional set of tests. These new tests differ from our default pipeline in that we use the simpler to calculate Gaussian bias for both data and simulations. This will result in a less accurate calculation of the lensing spectrum for our data, but it treats all calculations equally. If the resulting PTEs from this set of null tests are lower than their counterparts in Table 2 then we have evidence that the realization-dependent bias subtraction is the source of high PTEs in our data split null tests. When we performed this new test the results showed that nearly all the PTE values decreased (including all 12 of the worst $\chi^2$ PTEs) as is consistent with this hypothesis.

As for the implications of this on our final results, not using a realization-dependent bias subtraction for simulations may be resulting in slightly larger error bars and a more conservative estimate of our detection significance. As an approximate estimate of how big this effect might be, we look at the distributions of $\chi^2_{null}(b)$ values for each patch and estimator to see how much the standard deviation of the distribution of these $\chi^2_{null}(b)$ changes. The effect varies for each estimator, but on average we see a 4% change in the standard deviation of the distribution when comparing results with and without the realization-dependent calculation. This is a small effect, on the order of the uncertainty from using a finite number of simulations, and so we are confident that the results in Table 2 still serve as an acceptable check on unknown systematic biases in the rest of our analysis pipeline.

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