Development Of Cryogenic Detectors For Neutrinoless Double Beta Decay Searches

Mattia Beretta \(^1\) and Lorenzo Pagnanini \(^2\)

\(^1\) University of California Berkeley, Berkeley, California, US; mattia.beretta@berkeley.edu
\(^2\) Gran Sasso Science Institute, L’Aquila, Italy; lorenzo.pagnanini@gssi.it

Abstract: Searching for neutrinoless double beta decay is a top priority in particle and astroparticle physics, being the most sensitive test of lepton number violation and the only suitable process to probe the Majorana nature of neutrinos. In order to increase the experimental sensitivity for this particular search, ton-scale detectors operated at nearly zero-background conditions with a few keV energy resolution are required. In this scenario, cryogenic detectors have proven effective in addressing many of these issues simultaneously. After long technical developments, the CUORE experiment established the possibility to operate large scale detectors based on this technology. Parallel studies pointed out that scintillating cryogenic detectors represent a suitable upgrade for the CUORE design, directed towards higher sensitivities. In this work, we review the recent development of cryogenic detectors, starting from the status of the art and outlining the path toward next-generation experiments.

Keywords: Neutrinoless Double Beta Decay, Lepton Number Violation, Rare event search, Cryogenic detector

1. Introduction

Particle detectors exploit several mechanism to convert an energy deposition from ionizing radiation into a measurable quantity. The most widely used technologies measure either the ionization produced in the detector volume or scintillation signals excited in the radiation-absorbing material by the interacting particles. However, the energy detectable via these channels is only a small fraction of the total energy deposit, as the largest part is converted in lattice vibrations (i.e. heat) and escapes detection. A possible solution to increase the sensitivity consists in using a detector able to measure the vibration quanta (i.e. phonons) produced by an interaction: a cryogenic calorimeter.

In a very simplified model, a cryogenic calorimeter can be sketched as an absorber, usually a diamagnetic crystal, attached to a phonon sensor. When a particle releases energy in the absorber, its temperature increases and phonons are produced in its lattice. The phonons propagate in the absorber and are converted into a measurable signal by the sensor, acting as a thermometer. Each energy deposit in the absorber \(E_{\text{Dep}}\) induces a temperature increase \(\Delta T\), given by \(\Delta T = E_{\text{Dep}}/C\), where \(C\) is the absorber capacity. To increase the sensitivity of this measurement method, \(C\) has to be minimized. This goal is achieved by keeping the absorber at temperature \(\sim 10 \text{ mK}\) by means of a thermal machine, usually a dilution refrigerator. In these conditions, in fact, \(C \propto (T/T_D)^3\), where \(T_D\) is the Debye temperature of the material. The energy resolution of such detectors is their main characteristic, and it is only limited by the thermal noise and by eventual imperfection of thermalizations. Since the average energy of a phonon is \(\sim \mu\text{eV}\), the average number of phonons created by a \(\sim\text{MeV}\) interaction is extremely large, allowing only small statistical fluctuation of the information carriers. Moreover, different materials can be used as absorbers, providing the possibility to investigate different processes through different strategies. The main downsides of these technique are the inability to natively perform multi-messenger measurements and the need for high-power cooling devices to maintain the cryogenic temperatures. The former features translates into the inability to identify interacting...
particles producing undesired backgrounds, while the latter strongly limits the possibility to operate large detector masses with an easily scalable architecture.

The major running experiment based on technique is CUORE (Cryogenic Underground Observatory for Rare Events), built with TeO\textsubscript{2} crystals to search for the 0\(\nu\)\(\beta\beta\) of \(^{130}\text{Te}\). With respect to the native size limitation of the cryogenic calorimeters, the experience of CUORE demonstrated that these detectors can be built with masses on the tonne scale, paving the way to the development of next generation calorimetric detectors. During CUORE development, numerous efforts have been devoted to select and use clean materials to build the detector system, reducing significantly the level of background. At this stage, the CUORE limiting factor on this side is the degraded \(\alpha\)-particles background, which can be reduced only to a certain extent. To overcome this limitation, hybrid thermal-scintillation detectors have been identified as suitable candidates. Since \(\alpha\) and \(\beta\) particles present different scintillation mechanism, the access to a scintillation light readout allows an efficient background tagging. Such design has been carefully investigated and put to test in recent years, leading to the definition of a new path towards a next generation cryogenic detector for the search of neutrinoless double beta decay: CUPID (CUORE Upgrade with Particle IDentification).

In this work, the steps leading to the CUORE design will be described, together with a discussion of the most recent developments of cryogenic calorimeter techniques directed to the next generation of experiments.

2. The experimental search for Neutrinoless Double Beta Decay

The incontrovertible evidence of massive neutrinos has been given by the measurement of their flavour oscillations [1–4]. These results demonstrate that the electroweak sector of the Standard Model is incomplete and that new Physics is necessary to correctly model the observed phenomena. In this landscape, a unique role is played by the Neutrinoless Double Beta Decay (0\(\nu\)\(\beta\beta\)). 0\(\nu\)\(\beta\beta\) is a special case of the more general double beta decay (\(\beta\beta\)) of even-even nuclei. This process is a rare nuclear transition in which an initial nucleus (\(A,Z\)) decays to a member (\(A,Z+2\)) of the same isobaric multiplet with the simultaneous emission of two electrons. According to the Standard Model (SM), \(\beta\beta\) must obey lepton number conservation. As a consequence, the SM final state comprehends two antineutrinos and is labelled as a two neutrino double beta decay (2\(\nu\)\(\beta\beta\)). In this process, the two emitted electrons carry a fraction of the total energy of the transition, called Q-value (\(Q_{\beta\beta}\)). Such decay mode is shared by all the \(\beta\beta\) candidate isotopes, and is characterized by half lives \(\geq 10^{18}\)\(\text{y}\). On the other hand, assuming that neutrinos have to be explained by beyond the SM phenomenology, \(\beta\beta\) can happen with only electrons in the final state, in the so-called 0\(\nu\)\(\beta\beta\) mode. Being an exotic variant of an already rare process, 0\(\nu\)\(\beta\beta\) has expected live times longer than \(10^{27}\)\(\text{yr}\). This extremely rare process is of great interest since, if detected, would simultaneously prove the existence of lepton number-violating processes, state the Majorana nature of neutrinos and provide a value to their absolute mass scale [5,6].

The experimental search of 0\(\nu\)\(\beta\beta\) relies on the detection of the two electrons emitted in the process. Since the recoil energy of the nucleus is negligible, the two electrons carry a total kinetic energy equal to \(Q_{\beta\beta}\). The expected signature is therefore a peak in the sum energy spectrum of the electrons centred around the \(Q_{\beta\beta}\). The energy region for this search is usually referred to as the Region of Interest (ROI), and its width is a multiple of the full width at half maximum energy resolution of the used detector, evaluated at the \(Q_{\beta\beta}\). The peak to be searched has to be distinguished from two main background categories. On one side, spurious events due to external radioactivity can hide the peak. On the other, the 2\(\nu\)\(\beta\beta\) continuous spectrum smeared by the experimental resolution can leak in the ROI. The latter background category is unavoidable, since it comes from the 0\(\nu\)\(\beta\beta\) source itself. The possibility to detect the 0\(\nu\)\(\beta\beta\) signal depends on different detector parameters. In particular the energy resolution (\(\Delta\)) and the background level (\(B\)) in the ROI play a crucial role in determining the effectiveness of a given experimental strategy. The performances of a given 0\(\nu\)\(\beta\beta\) detector are parameterized with the experimental sensitivity, \(F_{\beta\beta}^{0\nu}\), defined as the process half-life corresponding to the maximum signal that can be observed at a given statistical confidence level (CL). At 1\(\sigma\) level this is given by:
where \( \eta \) is the isotopic abundance of the candidate isotope, \( \epsilon \) is the detection efficiency, \( T_{\text{mis}} \) is the measurement time and \( M \) is the total detector mass. The expression in Equation 1 holds when the total background level is not compatible with zero. Such condition is met when \( M \cdot T_{\text{mis}} \cdot B \cdot \Delta > 1 \). When the experiment parameters do not satisfy this boundary, the sensitivity is better represented assuming \( B \sim 0 \), resulting in the following expression:

\[
F_{0^{\nu}D}^{0^{\nu}D}(ZB) = \ln 2 \frac{\eta \epsilon N_{\text{Av}}}{A} \sqrt{\frac{T_{\text{mis}} M}{B \Delta}} \quad (68\% \text{ C.L.})
\]

where \( n_L \) is a constant depending on the chosen confidence level and on the actual number of observed events. In this condition sensitivity is directly proportional to time and mass, making it possible to scale up the experiment reach by either increasing the mass or extending the measurement period [5].

Equations 1 and 2 summarize efficiently the most important design criteria for \( 0^{\nu}\beta\beta \) detectors:

- minimization of the continuous background (i.e. lowering \( B \) factor), achievable by:
  - placing experiment underground, in order to reduce the cosmic ray contribution to experimental background;
  - building the detector with radiopure materials, in order to minimize the \( \gamma \) and \( \beta \) contribution to background;
  - cleaning the surface of materials from radioactive contaminations, in order to reduce the degraded particle contribution to background;
  - shielding of the detector active volume with lead and copper layers, in order to reduce the external and setup radioactivity;
  - developing particle identification techniques, in order to discriminate degraded particle from electrons signals;
  - choosing a \( 0^{\nu}\beta\beta \) candidate isotope with high \( Q_{\beta\beta} \), in order to reduce \( \beta \) and \( \gamma \) events from the ROI and enhance the \( 0^{\nu}\beta\beta/2^{\nu}\beta\beta \) ratio;

- observation of large isotope mass (i.e. increasing \( M \) factor), achievable by:
  - choosing a \( 0^{\nu}\beta\beta \) candidate isotope with high natural isotopic abundance (high \( \eta \));
  - choosing a detector technology that allows easy mass scalability, that is to say possibility to have high masses without huge technological issues;

- achieve good energy resolution (i.e. decreasing \( \Delta \) factor), to reduce the \( 2^{\nu}\beta\beta \) background in the ROI;

- long time of observation (i.e. increasing \( T_{\text{mis}} \) factor) achievable by choosing stable detectors with low maintenance issues.

In this complex optimization problem, cryogenic calorimeters can play an important role, given their native characteristics [7]. During the last decades, this particle detectors have proven successfully in trying to address some of the key sensitivity issues, but no technology exist able to simultaneously fulfill all requirements.

3. The CUORE development

The CUORE experiment history, starting from its first prototype MiBETA, is an excellent summary of the efforts needed to optimize the cryogenic calorimeter approach to the search for \( 0^{\nu}\beta\beta \) [8].

Initially, the main difficulty to be addressed was increasing the reliability of these detectors both in operation time and in number of simultaneously operated channels. To minimize the efforts needed, \(^{130}\text{Te}\) was chosen as the isotope under study, given its high natural isotopic abundance (34.2% [9]). The MiBETA R&D allowed to operate initially a single crystal of TeO\(_2\) for one year [10], proving the
feasibility of this technique. After this initial proof of concept, a more complex array was designed and put to test, combining 20 crystals with different dimensions [11]. These steps paved the way to the MiBETA experiment [12], that solidified the previous results and promoted the possibility to operate a large array of cryogenic detectors. At this stage, background became an issue to be dealt with in the experimental optimization. The $2\nu\beta\beta$ induced background was strongly limited by the good energy resolution of these detectors, while the spurious background had to be addressed. To reduce cosmogenic background, these experiments were placed underground in the Gran Sasso National Laboratories (LNGS) [13–15], an infrastructure providing a 3600 m.w.e. shielding against cosmic rays. From the experimental results, the main spurious background contribution was identified in the degraded as. The signature of these events is a continuous spectrum below 9 MeV, unavoidable in experiments sensitive only to the energy deposition. In order to reduce this contribution as well as the general level of radioactivity, the materials building the detector and those directly facing it were selected through strict screening procedures. The goal was to identify the least contaminated materials, then chosen to build the future experiments. In particular, OFC copper was selected for the detector holder, and PTFE was used to hold the crystals in place. To directly address the issue of degraded as, the surface of all the materials was treated to remove the external layers, responsible for the majority of these events. Also the detector shields have been optimized and chosen as a dual copper/lead layer. To reduce the bremsstrahlung emission from $\beta$ rays, characteristics of standard lead shieldings, a ancient roman lead shield was built, characterized by low content in $^{210}\text{Pb}$ [16].

Once these improvements were defined, the first step toward the final CUORE design has been the CUORICINO array [17], simultaneously operating 62 crystal with different geometries. The results obtained with this experiment [18,19] allowed to select a final shape and configuration for the detector. The chosen design was based on 5x5x5cm$^3$ cubical $\text{TeO}_2$ crystals arranged in towers composed by 13 planes combining 4 crystals each. The design was finalized and operated as the CUORE-0 experiment [20], which served as general test for the CUORE assembly line. The CUORE-0 detector is, in fact, one of the 19 towers now operating in the CUORE cryostat. Its operation allowed to test and finalize both the hardware and software tools needed for the ongoing CUORE operation and analysis [21,22].

Parallel to the optimization of a multi-crystal array of cryogenic calorimeters, significant steps have been made towards the development of a cryostat. The target device had to keep $\sim$1 ton of crystals cooled around 10 mK, while keeping at a minimum the amount of radioactive contaminants in its building materials. The design process led to the realisation of the CUORE cryostat, a one-of-its-kind machine built to satisfy these impressive goals [23]. Among different optimisations, the aforementioned material selection and treatment allowed to minimise the possible backgrounds of the experiment.

The outcome of this 2-decade long optimization process is the now running CUORE experiment, which established the most competitive limit on $^{130}\text{Te} \ 0\nu\beta\beta$ half-life [24].

4. Beyond the CUORE sensitivity

The technical results obtained by CUORE showed that it is possible to run a tonne-scale bolometric experiment, overcoming the mass scalability limitation related to the use of a dilution refrigerator. The next-generation experiments aim to explore the whole inverted hierarchy of neutrino masses and a relevant fraction of the normal one, reaching a sensitivity $> 10^{27}$ yr on the $0\nu\beta\beta$ half-life [9,25,26]. To achieve this goal with cryogenic calorimeters, the CUORE background level must be reduced by two orders of magnitude, exploiting a particle identification technique to discriminate degraded a particle from electron signals.

In the search for a novel approach, the scintillation-based detectors have proven to be effective in addressing this issue. The combination of these two techniques, resulting in scintillating bolometric detectors, was proposed in 1989 for solar neutrino experiments [27]. The first application $0\nu\beta\beta$ searches with a background suppression were performed with crystal facing standard light detectors (LD), such as photodiodes [28], and where limited by the technical difficulties in using standard LDs at cryogenic temperatures. An innovation in this field was the proposal to use cryogenic calorimeters as custom
low-temperature LDs [29]. This idea led to the development of new possible detector design [30]. The main advantages of this approach is the sensitivity shown by these calorimeters. With respect to standard LDs, these devices have higher photon detection efficiencies in a wide region of photon wavelength. On the other hand, they cannot be applied in single-photon counting, due to their low native gain, and are characterised by slower response time with respect to standard photo-detectors (ms versus ns or even less). Different studies have been performed exploring the possibilities of this technique [31–33], proving the background rejection capabilities and the possibility to investigate different isotopes. This success paved the way for the construction of two demonstrators, which allowed to test different crystals and to set limits of $0\nu\beta\beta$ half-lives for two isotopes: CUPID-0 ($^{82}$Se) and CUPID-Mo ($^{100}$Mo).

The excellent performance of CUORE, CUPID-0 [34,35] and CUPID-Mo [36,37] laid the foundation for a CUORE Upgrade with Particle Identification, i.e. CUPID [38,39]. The main goal of the CUPID project is the design and operation of a tonne-scale detector to reach a sensitivity of $10^{27}$ yr on $0\nu\beta\beta$ [9].

The progress in the development of cryogenic calorimeters is summarised in Figure 1, where we show for each experiment the exposure and the ROI background integrated in a detector FWHM, both corrected for the efficiency and expressed in unit of moles of the isotope under study [40]. These variables are calculated using the data in Table 1, extracted from the latest published data from the experiments. The evolution towards better performances of the CUORE precursors shows the results of the technical developments performed during the CUORE design optimization. The experiment were increasingly bigger, while continuously reducing the intrinsic background levels. Unfortunately, both the $^{130}$Te characteristics and the unavoidable degraded $\alpha$ background prevented this technical approach from reaching the zero-background regime. Upgrading the CUORE design using scintillating calorimeters with dual heat-light readout will allow reaching this goal. The pilot experiments (CUPID-0 and CUPID-Mo) were able to cross such boundary, reaching world-leading performances even with small exposures. The ongoing CUPID program is the next step towards the scale-up of the scintillating calorimetric technique to the CUORE scale.

Table 1. Performance of different $0\nu\beta\beta$ experiments based on cryogenic calorimeters. The data are measured for all the experiments except for CUPID, where the best prediction of performances at the end of the operation time is reported. CUORE data reflect the latest published results, therefore these performances are expected to change as its data taking progresses.

| Experiment | Exposure [kg yr] | Resolution [keV] | Background [cnts/(kev kg yr)] | Efficiency [%] | Reference |
|------------|-----------------|-----------------|-------------------------------|----------------|-----------|
| MiBETA     | 0.66            | 8 ± 1           | $0.5^{+0.4}_{-0.3}$           | 84.5           | [12]      |
| CUORICINO  | 19.75           | 6 ± 0.5         | 0.2                           | 82.8 ± 1.1     | [18]      |
| CUORE-0    | 9.8             | 5.1 ± 0.3       | (5.8 ± 0.4) stat. ± 0.2 syst. 10^{-2} | 81.3 ± 0.6     | [21]      |
| CUORE      | 103.6           | 7.0 ± 0.4       | (1.38 ± 0.07) 10^{-2}         | 77.3 ± 0.1     | [24]      |
| CUPID-0    | 5.09            | 20.0 ± 0.3      | $3.5^{+0.9}_{-0.8}$ 10^{-3}    | 70 ± 1         | [35]      |
| CUPID-Mo   | 0.48            | 7.7 ± 0.7       | $3^{+2}_{-3}$ 10^{-3}         | 68 ± 1         | [41]      |
| CUPID      | 1000            | 5               | $10^{-4}$                     | 64             | [25]      |
Figure 1. Comparison of the performances of the different $0\nu\beta\beta$ experiment based on cryogenic calorimeters described in this work. The $x$- and $y$-axis report the exposure and the ROI background integrated in a single detector FWHM respectively. These values are both corrected for the detection efficiency and expressed in terms of moles of $0\nu\beta\beta$ isotope under study. The variables are defined according to [40], and are calculated using the references reported in Table 1. The black line represents the boundary between the non-zero background regime (upper side) and the zero-background regime (lower side). The cluster of red points refers to the development history of CUORE. The steps made towards reducing the background and increasing sensitive exposure are clearly visible. It is also clear that the developed technical solution is not enough to reach the zero-background region, where the increase in sensitive exposure obtained with CUORE would be more effective. It has to be pointed out that CUORE is the only running experiment in this collection, therefore its position in this plane is expected to change with time as more data are collected. The blue points show the position of the CUPID demonstrators (CUPID-Mo and CUPID-0). Their smaller exposures are compensated by a much lower background level, obtained thanks to the combined heat-light readout. The magenta point shows the predicted performances for CUPID, foreseen to combine the best characteristics of the previous development steps. The error bars are present on each point but are hidden by the point marker.

4.1. The CUPID challenge

The CUORE upgrade to achieve CUPID objectives passes through three fundamental steps:

- increase the $0\nu\beta\beta$ emitters via isotopic enrichment;
- active rejection of $\alpha$s and surface backgrounds in detector materials;
- further reduction (compared to CUORE) in the $\gamma$ backgrounds by careful material and isotope selection, and an active veto for muon-induced events.

In the last ten years, different isotopes (see Fig. 2) and approaches were investigated for CUPID. Background rejection with scintillation, Cherenkov radiation, ionization, and pulse-shape discrimination was evaluated, and novel materials and sensor technologies where tested [42,43]. The
Figure 2. Expected energy signature in the two-electron sum-energy spectrum for the nine most suitable double-beta emitters. These are compared with background energy markers related to the maximum γ energies of the 238U and 232Th chains and the maximum β energy of the 238U chain. The main experiments are also mentioned in relation with their selected nucleus. For essentially technical reasons, most searches investigate the three least favourable isotopes. The isotope selected for the CUPID baseline is 100Mo. Figure reprinted from [25].

activities carried out in the last years to design a next-generation 0νββ bolometric experiment are briefly summarised here, divided according to the isotope under investigation.

**130Te.** Large scale production of high quality TeO₂ crystals was already demonstrated within the CUORE experience. However, the production of enriched crystal has to be validated to certify the energy resolution as well as the internal contaminations. This work has started on 2015, producing and operating two highly-enriched TeO₂ crystals (435 g each) [44]. This first test gave very satisfactory results, showing an energy resolution of 6.5 and 4.3 keV FWHM at 2615 keV, respectively. The only observable internal radioactive contamination came from 238U (15 and 8 µBq/kg, respectively). The internal contamination of the most problematic nuclei for 0νββ, 226Ra and 228Th, are both evaluated as <3.1 µBq/kg and <2.3 µBq/kg respectively. Thanks to the readout of the weak Cherenkov light emitted by β/γ particles by means of Germanium Neganov-Luke [45] bolometric light detectors, it was possible to perform an event-by-event identification of β/γ events with a 95% acceptance level, while establishing a rejection factor of 99.99% for α particles. Alongside this study, silicon Neganov-Luke amplified light detectors were also successfully tested on a 1×1×1 cm³ TeO₂ crystal, obtaining a full rejection (4.6 σ) of the α-particles [46]. Other previous results can be found in Refs. [47–55]. Despite the excellent results obtained, there are still two critical factors to be dealt with:

- the emitted Cherenkov light at the 130Te Qββ is very small (∼ 100 eV), therefore the energy RMS resolution of the light detectors must be less than 20 eV, and this cannot currently be guaranteed;
- the γ-background at the 130Te Qββ is one order of magnitude higher with respect to the CUPID goal.

**82Se.** This isotope was deeply investigated within the LUCIFER (Low Background Installation For Elusive Rates) program, establishing from scratch the ZnSe powder synthesis and purification protocols [56]. The crystals growth was refined, studying by means of cryogenic tests the properties of dozens of ZnSe samples [57–60]. Finally 24 ZnSe crystals, 95 %-enriched in 82Se were produced and mounted in CUPID-0 [61]. The CUPID-0 demonstrator has taken data from 2017 to 2019, demonstrating a complete rejection for α-particle exploiting a light-assisted particle discrimination. With these tagging capability, the delayed coincidences between 212Bi α-decays and 208Tl β-decays could be identified, thus removing from the measured spectrum the 208Tl β-events falling in the 82Se ROI. Combining
the excellent particle identification with the delayed coincidence analysis, CUPID-0 has archived a background index of \(3.5^{+1.0}_{-0.9} \times 10^{-3}\) counts/(keV·kg·yr), the lowest value ever measured in a cryogenic calorimeter[35]. This important result established the potential of bolometers for a next-generation experiment, setting also the most stringent limit on \(^{82}\text{Se} \, 0\nu\beta\beta\) half-life \[35\]. Finally, a full modellization of the measured spectrum has also been performed, demonstrating that the main residual background in the ROI is due to muon-induced events \[62\]. The deep understanding of the data allowed also a high precision measurement of \(^{82}\text{Se} \, 2\nu\beta\beta\) \[63\] and the extraction of limits for other rare processes \[64–66\]. The critical point of this technique is the mass production of high-quality ultra-pure crystals, which still demands an extensive R&D effort.

\(^{100}\text{Mo}\). Large mass (~1 kg), high optical quality, radiopure \(^{100}\text{Mo}\)-containing molybdate crystals have been produced and used to develop high-performance single detector modules based on 0.2 - 0.4 kg scintillating calorimeters. Even if the production of such crystals was not established as TeO\(_2\) ones, in a relative short amount of time impressive performances were achieved both in term of energy resolution (4–6 keV at 3 MeV) and radiopurity (10 \(\mu\)Bq/kg of \(^{232}\text{Th}\) and \(^{226}\text{Ra}\)). Moreover, the rejection of the \(\alpha\)-induced dominant background above 2.6 MeV is better than 8\(\sigma\). An extensive R&D has been carried out to select the best candidate crystal for a next generation experiment in the framework of LUMINEU project and by the AMoRE collaboration \[67\], converging on Li\(_2\)MoO\(_4\) as best candidate\[68,69\]. The most advanced example of this technology is the CUPID-Mo experiment. It consists of a 2.6 kg array of 20 enriched Li\(_2\)MoO\(_4\) crystals, arranged in 4 towers, operated as cryogenic calorimeters for more than one year. Bolometric Ge light detectors are interleaved between the crystals, resulting in all but the top elements of the towers facing a LD both at the top and the bottom \[70\].

The experiences and information acquired carrying out the aforementioned activities allowed to identify enriched Li\(_2\)MoO\(_4\) crystals as the best candidates for the next-generation CUPID experiment, given their excellent performances in terms of energy resolution, radiopurity and particle identification. Based on the available information, a design for the CUPID detector has been defined \[25\]. The different specification are listed in Tab. 2. The predicted performances of the experiment have been conservatively estimated taking into account all the information acquired during the investigation of different approaches and mainly by the CUORE, CUPID-0 and CUPID-Mo experiments. One of the main constraint of this design is the requirement for CUPID to be fully compatible with the existing CUORE infrastructure in terms of mechanical coupling, cryogenics, readout, and DAQ features. This characteristic is mandatory to boost the time schedule and to have the experiment running before 2030.

In the current design, the background index reduction is limited by the not resolved fraction of the two-neutrino double-beta decay pile-up on the rising edge of the bolometric signal. Such effect is due to the relatively short \(^{100}\text{Mo} \, 2\nu\beta\beta\) half-life, combined with its high isotopic abundance, and the slow response time of the bolometric detectors. New methods are being developed in order to study and tackle this issue \[71\], and a further improvement of the pile-up rejection will be achieved by combining faster sensor (100 \(\mu\)s) with new analysis techniques based on Principal Component Analysis and Single Value Decomposition \[42,72,73\].

4.2. An alternative to cryogenic calorimeters

As mentioned above, the scintillation-based detectors are suitable candidates for the search of \(0\nu\beta\beta\). They can natively perform active background reduction and are easier to scale up than cryogenic calorimeters, since they can be operated at less extreme temperature. The limit to this technology the energy resolution achievable by the light signal. This limit comes from the statistical fluctuation in the number of collected photons, limited by the light collection efficiency of the chosen scintillator-photodetector system. Such limit can be overcome defining new design for performing scintillation detectors. Such development is centered on the improvement in resolution, and has the target of FWHM \(\leq 0.02 \cdot Q_{\beta\beta}\) to ensure at least a limited effect (\(\leq 10\%\)) of \(2\nu\beta\beta\) on the background. For the chosen design suitable scintillators containing \(0\nu\beta\beta\) candidate isotopes have to be chosen. In such context, suitable stands for highest possible light yield and fast scintillation time. With
Table 2. Main parameters of the conservative baseline CUPID detector design.

| Parameter                        | Baseline                                      |
|----------------------------------|-----------------------------------------------|
| Crystal                          | Li$_2$MoO$_4$                                 |
| Crystal size                     | $4.5 \times 4.5 \times 4.5$ cm$^3$            |
| Crystal mass (g)                 | 241                                           |
| Number of crystals               | 1500                                          |
| Number of light detectors        | 1500                                          |
| Detector mass (kg)               | 362                                           |
| $^{100}$Mo mass (kg)             | 200                                           |
| Energy resolution FWHM (keV)     | 5                                             |
| Background index (counts/(keV·kg·yr)) | $10^{-4}$                                    |
| Containment efficiency           | 79%                                           |
| Selection efficiency             | 90%                                           |
| Livetime                         | 10 years                                      |
| Half-life limit sensitivity (90%) C.L. | $1.5 \times 10^{27}$ y                       |
| Half-life discovery sensitivity (3$\sigma$) | $1.1 \times 10^{27}$ y                      |
| $m_{\beta\beta}$ limit sensitivity (90%) C.L. | 10 – 17 meV                                |
| $m_{\beta\beta}$ discovery sensitivity (3$\sigma$) | 12 – 20 meV                                |

Such characteristics, the detector would not be limited by the crystal properties, allowing major improvements based on readout system upgrades. Such improvements will be related to the increase in light emission, optimization of photon extraction and optimization of readout chain. For the increase in light emission the operation at cryogenic temperatures provides an effective strategy. When the vibrational modes of a scintillating material are deactivated, in fact, the vibrational non-radiative de-excitation is damped. As a consequence, the light emission increases [74]. On photon extraction, different wrapping strategies can be implemented, surrounding the crystal with materials capable of re-direct the outgoing scintillation photons toward the photodetector. Lastly, the choice of an efficient photon detector is the most important aspect to be considered, since at this first measurement stage the actual level of the collection efficiency is determined. As a consequence detectors with high quantum efficiency have to be preferred, in order to obtain better performances [75]. Also consideration of gain fluctuations, non uniform efficiency and readout noise have to be considered, since all these aspects take part in spoiling the resolution. The FLARES (Flexible Light Apparatus for Rare Events Search) project, tried to follow this concept. It proposed the development of a detector based on the use of Silicon Drift Detectors (SDD) to read the light emitted by large scintillation crystals, cooled at 120K [76,77]. SDDs are characterized by low noise and high quantum efficiency, while the scintillators containing $^{0}\nu\beta\beta$ candidates can be enhanced in their performances by the low temperatures.

Considering a completely different approach, the resolution problem can be addressed by selecting more performing scintillating materials. In this framework, the scintillating nanocrystals play an important role. These new generation of compounds, in fact, is characterized by extremely high light emission, and they can be designed to work at a certain wavelength, thus making the optimization of their readout chain easier [78,79]. In addition, the absence of non-radiative de-excitation channels makes the radiative recombination extremely quick, with scintillation emission time on the order of few ns. At current status, different nanoscintillators are available, in terms of different structures and constituting elements. This large choice possibility makes them versatile, since it is possible to choose the needed materials with the needed emission spectrum to fit the demands of a certain application. In particular, some of these materials can be built using elements with isotopes candidate to $^{0}\nu\beta\beta$, such as Te or Se. Different studies have been performed with QDs used as doping for liquid scintillators, since these materials provide both a wavelength shifter and a source for the $^{0}\nu\beta\beta$ [80–82]. On the other hand, using these materials simultaneously as radiation emitters and absorbers presents more difficulties. The accumulation of great masses of nanocrystals is, in fact, problematic, since the self-absorption limits the light output. In addition, such compounds are produced as powders,
needing a matrix to be arranged in more useful structures. Such difficulties prevented their application to the scintillation-based detection of radiation. In this framework, the ESQUIRE (Experiment with Scintillating QUantum dots for Ionizing Radiation Events) project proposes a possible pathway to the development of new scintillation detectors, aimed to a final application to the search of $0\nu\beta\beta$ [83]. ESQUIRE R&D work focuses on the selection of different QDs with optical characterization, followed by a direct scintillation measurement performed with high sensitive solid state photon detectors. The initial work allowed to demonstrate the possibility to apply nanocrystals as fast scintillators [84], validating a part of its initial goals.

5. Conclusions

Developing $0\nu\beta\beta$ detectors forces the design of innovative solutions to overcome the congenital difficulties of this frontier research. During the last 30 years, the application of cryogenic detectors in this field rapidly progressed thanks to a continuous R&D work culminated in the CUORE construction and operation. This experiment is currently demonstrating the possibility to operate 1000 crystal as cryogenic calorimeters in a single cryostat, paving the way to a new generation of $0\nu\beta\beta$ detectors. The next step in this line will be the CUPID experiment. Its development is ongoing and relies both on the CUORE experience and on the CUPID-0 and CUPID-Mo prototypes. The new challenges to be overcome, especially the $2\nu\beta\beta$ pile-up, are currently being tackled by combined new hardware and analysis solutions to improve energy and time resolution. The long experience achieved also pointed out the issues that cannot be solved within the current CUORE infrastructure, opening the investigation to other possible solutions for a next-generation $0\nu\beta\beta$ experiment. It appears clearly then that the development of cryogenic calorimeters is a challenging task, capable to produce innovation in the radiation detector landscape.

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