Landau theory for magnetic and structural transitions in CeCo$_{0.85}$Fe$_{0.15}$Si

William Gabriel Carreras Oropesa$^{1}$, Víctor F Correa$^{1,2}$, Julián G Sereni$^{1,2}$, Daniel J García$^{1,2}$ and Pablo S Cornaglia$^{1,2}$

$^1$ Centro Atómico Bariloche and Instituto Balseiro, CNEA, 8400 Bariloche, Argentina
$^2$ Consejo Nacional de Investigaciones Científicas y Técnicas (CONICET), Argentina

E-mail: william.carreras@ib.edu.ar

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Abstract
We present a phenomenological analysis of the magnetoelastic properties of CeCo$_{0.85}$Fe$_{0.15}$Si at temperatures close to the Néel transition temperature $T_N$. Using a Landau functional we provide a qualitative description of the thermal expansion, magnetostriction, magnetization and specific heat data. We show that the available experimental results (Correa et al 2016 J. Phys.: Condens. Matter 28 346003) are consistent with the presence of a structural transition at $T_s \gtrsim T_N$ and a strong magnetoelastic coupling. The magnetoelastic coupling presents a Janus-faced effect: while the structural transition is shifted to higher temperatures as the magnetic field is increased, the resulting striction at low temperatures decreases. The strong magnetoelastic coupling and the proximity of the structural transition to the onset temperature for magnetic fluctuations, suggest that the transition could be an analogue of the tetragonal to orthorhombic observed in Fe-based pnictides.

Keywords: magnetism, magnetostriction, Landau functional, phase transitions

(Some figures may appear in colour only in the online journal)

1. Introduction

Ce based compounds have attracted considerable attention over the years due to their wide range of physical properties which include unconventional superconductivity [1], heavy fermion behavior [2], magnetism, non-Fermi liquid behavior and quantum phase transitions [3]. In these compounds the properties depend strongly on the hybridization of the 4f Ce$^{3+}$ orbital to the conduction band and on the dimensionality. The crystalline environment of the Ce$^{3+}$ ions determines the degree of localization of the 4f electrons and the magnetic interactions between them. As a result, these systems can present magnetic ground states with ordered local magnetic moments or heavy fermion behavior where the magnetic moments are Kondo screened. External pressure or chemical doping may induce a transition between these phases. The role of the dimensionality manifests itself in, e.g. the layered 115 compounds, CeMnS (M = Rh,Co, Ir) where decreasing the coupling between layers leads to an increase in the superconducting transition temperature [4–7]. These compounds share a number of common features with the cuprate superconductors that have made them a proxy in the quest to understand high temperature superconductivity [8].

The rich variety of behavior presented by Ce-based compounds seems to be, in general, dominated by electron–electron correlations. In Ce mono-pnictides, however, strong signatures of the coupling between the magnetic and elastic degrees of freedom have been reported [9–12]. More recently, in the CeCo$_{0.85}$Fe$_{0.15}$Si compound, a strong signature in the thermal expansion ($\Delta L / L \sim 10^{-4}$) was observed at the magnetic transition [13], indicating the presence of a significant magnetoelastic coupling.

CeCo$_{1-x}$Fe$_x$Si compounds range from CeCoSi, which presents a second order transition to an antiferromagnetic state at $T_N = 8.8$ K, to CeFeSi which is a paramagnetic Fermi liquid. As the concentration of Fe (y) increases, the Néel temperature $T_N$, as deduced from the peak in the specific heat at the transition, decreases and the peak becomes weaker (see figure 1(a)). The behavior of the specific heat [14] suggests a chemical pressure effect due to the substitution of Co by...
Fe. This leads to a suppression of the Néel transition and the development of a bump in a way that resembles a dimensional crossover from 3D to 2D magnetism [15]. The antiferromagnetism is completely suppressed (see figure 1(b)) for $y \gtrsim 0.23$ [14]. Interestingly, an anomaly in the specific heat at a temperature $T_A > T_N$ was identified in [14] which was interpreted as an onset of large magnetic fluctuations in the paramagnetic phase near the Néel transition.

In the $y = 0.15$ compound a strong dependence of the longitudinal linear expansion on the magnetic field was also observed (see figure 1(c)). A peak in the thermal expansion coefficient, which was interpreted as stemming from a structural transition, is obtained at a temperature $T_s \sim T_N$ while another peak is observed at the Néel transition (see figure 1(d)). Both peaks show a strong magnetic field dependence, while the peak at $T_N$ shifts to lower temperatures as the magnetic field is increased, the peak at $\sim T_s$ shifts to higher temperatures. Figure 1 summarizes the main experimental observations for the $y = 0.15$ Fe doping concentration [13]. The magnetostriction presents perhaps the more puzzling behavior (see figure 1(e)). The shift to higher temperatures of the structural transition with increasing magnetic field would seem to imply an enhanced structural distortion at low temperatures as the magnetic field is increased. The experimental results present precisely the opposite behavior at low temperatures.

Motivated by these recent experiments on the magnetoelastic properties of polycrystalline CeCo$_{0.85}$Fe$_{0.15}$Si [13] that show a strong magnetostructural coupling and suggest the presence of a structural transition, we analyze the possibility of the presence of such structural transition to explain the observed experimental data. To that aim we propose a Landau free energy to describe a magnetic transition and a structural transition including a magnetoelastic coupling. The qualitative agreement obtained with the available experimental data indicates that the latter is consistent with the presence of a structural transition at a temperature $T_s \sim T_A \gtrsim T_N$.

2. Landau theory

For the doping $y = 0.15$ the material shows a clear Néel transition at $T_N \simeq 6.5$ K. The anomaly in the specific heat evolves continuously from a textbook transition in the $y = 0$
compound until it vanishes at a doping $y \sim 0.23$. The linear thermal expansion coefficient $\alpha_L$ presents a wide peak ranging from $T \sim T_N$ to $T \sim 13$ K that in the presence of an external magnetic field it splits into two peaks (see figure 1(d)).

To describe the magnetic transition under an external magnetic field we propose a Landau functional in terms of the staggered magnetization $m = m_A - m_B$ and a uniform magnetization $M = m_A + m_B$, where $m_A$ and $m_B$ correspond to two sublattices which are coupled antiferromagnetically. We also include an order parameter $\delta$ to describe a structural transition. The structural transition produces a lattice striction that for simplicity we assume proportional to $\delta$ ($\Delta L/L = \delta$). As usual we consider that it is possible to make a series expansion of the free energy in terms of the order parameters close to the transitions and consider the lowest order terms allowed by symmetry. The free energy in units of $E_0 = 50$ J mol$^{-1}$ can be written as

$$
\Phi = \Phi_m + \Phi_B + \Phi_x + \Phi_{\text{tm}},
$$

(1)

where the magnetic transition is described by

$$
\Phi_m = -a_m \left(1 - \frac{T}{T_N}\right) m^2 + b_m m^6 + c_1 (mM)^2 + \frac{1}{2\chi} M^2.
$$

(2)

Here the first two terms, where $a_m > 0$ and $b_m > 0$, correspond to the standard functional to describe a mean field second order transition. The third term with $c_1 > 0$ is the competition between the staggered and uniform magnetizations and the last term is the energy associated with a uniform magnetization.

$$
\Phi_B = k_1 m^2 B^2 - MB,
$$

(3)

with $k_1 > 0$, describes the lowest order coupling terms of the magnetic field to the magnetizations$^3$.

The structural transition is described by

$$
\Phi_x = -a_x \left(1 - \frac{T}{T_s}\right) \delta^2 + c_x \delta^3 + b_x \delta^4
$$

(4)

where $a_x > 0$, $b_x > 0$ and a finite $c_x$ sets the sign of the deformation $\delta$, $c_x > 0$ corresponding to a contraction ($\delta < 0$) below the transition temperature. For finite $0 < c_x \ll b_x$ the transition is weakly first order with a jump in the order parameter $\sim c_x/\beta_x$. Finally, for the magnetoelastic coupling we expect terms of the form $\gamma_n^\pm (M^2 \pm m^2) \delta^n$, for $n = 1, 2, \ldots$, where the positive sign corresponds to a local coupling $\propto (m_A^2 + m_B^2)$, and the negative sign to a non-local coupling $\propto m_A m_B$. As we will describe below, $n = 2$ terms with $\gamma_2^+ + \gamma_2^- < 0$ are crucial to describe the shift to higher temperatures of the structural transition as the magnetic field is increased, while the $n = 4$ term with $\gamma_4^+ \sim \gamma_4^-$ allows to explain the magnetostriction results at low temperature. The minimal magnetoelastic coupling terms that allow to describe qualitatively the available experimental data read

$$
\Phi_{\text{tm}} = \gamma_2 (m^2 + M^2) \delta^2 + \gamma_4 M^2 \delta^4 + \gamma_4 m^2 \delta^4,
$$

(5)

where $\gamma_4 \equiv \gamma_4^+ - \gamma_4^- \ll \gamma_4 \equiv \gamma_4^+ + \gamma_4^-$. We have taken here $\gamma_2^0 = 0$ because it revealed unnecessary for a qualitative description of the experimental data.

3. Determination of the Landau free energy parameters

In this section we obtain analytical solutions for the order parameters $\delta$, $m$, and $M$ that minimize the Landau functional of equation (1). To that aim we consider the solutions of the nonlinear set of equations $\partial \Phi/\partial \delta = 0$, $\partial \Phi/\partial m = 0$, and $\partial \Phi/\partial M = 0$. To set the functional parameters we make use of the main features of the available experimental data.

For small external fields ($B \to 0$) and high temperatures ($T > T_s > T_N$) we have $m = 0$, $\delta = 0$, $M \to 0$, and the magnetization $M$ is simply given by $M = \chi U B$. The experimental data shows an approximately linear behavior of $M$ at low fields and constant $\chi U$ in the temperature range where the transitions take place. We measure the magnetization per atom $M$ in terms of its saturation value $g_J \mu_B J$ and set $\chi U = 1/80$ T$^{-1}$ which is consistent with the saturation field obtained extrapolating the experimental data$^4$.

The structural transition temperature $T_s \sim 12.5$ K is determined by the high temperature peak in the linear thermal expansion coefficient ($\alpha_L$) in the absence of an external magnetic field. Guided by the behavior of $\alpha_L(T)$ as the magnetic field is increased, we assume that the broad peak observed in $\alpha_L(T)$ for $B = 0$ is composed by two peaks, one at $T_N$ and the other at $T_s$.

The structural transition temperature $T_s$ is defined as the temperature such that for $T < T_s$ the global minima in the free energy have finite distortion $\delta \neq 0$. Assuming a weak effect of the structural order on the uniform magnetization $M$, the structural transition temperature reads (for $c_x^2 \ll a_x b_x$)

$$
T_s(B) = \left(1 - \frac{\gamma_2^2 M^2}{a_x} + \frac{9c_x^2}{32a_x (b_x + \gamma_4 M^2)}\right) T_s
$$

(6)

$$
\sim \left(1 - \frac{\gamma_2^2 B^2}{a_x}\right) T_s
$$

which for $\gamma_2 < 0$ leads to an increase of the transition temperature with increasing magnetic field. The observed positive shift of $3K$ in $T_s$ for $B = 16$ T (see figure 1(d)) indicates $\gamma_2 \sim -9a_x$. For temperatures larger than the magnetic transition temperature, the structural order parameter can be described by a functional

$$
\Phi(T > T_N) \simeq -a_x(B) \left(1 - \frac{T}{T_s(B)}\right) \delta^2 + c_x \delta^3 + b_x(B) \delta^4
$$

(7)

$^4$ Hund’s rules applied to Ce$^{1+}$’s $4f$ electron result in $J = 5/2$ and a Landé factor $g_J = 6/7$. The lowest lying multiplet is however a doublet due to the presence of a crystal field.
Table 1. Landau functional parameters.

| Parameter                  | Value   |
|----------------------------|---------|
| Global energy scale $E_0$  | 50 J mol$^{-1}$ |
| Uniform susceptibility $\chi_U$ | 1/80 T$^{-1}$ |
| Temperature scale (magnetic) $T_N$ | 7.5 K |
| Temperature scale (structural) $T_s$ | 12.5 K |
| Functional term             | Value   |
| $-m^2(1-T/T_N)$             | $a_m$   | 0.5 |
| $m^4$                       | $b_m$   | 0.35 |
| $m^2M^2$                    | $c_1$   | 0.625 |
| $m^2h^2$                    | $k_1$   | $2.93 \times 10^{-4}$ |
| $-\delta^2(1-T/T_s)$        | $a_\delta$ | 3000 |
| $\delta^4$                 | $c_\delta$ | 10000 |
| $(m^2+M^2)\delta^2$        | $\gamma_m$ | $1.875 \times 10^{12}$ |
| $m^2\delta^4$              | $\gamma_m$ | $3.75 \times 10^{20}$ |

where

$$a_m(B) = a_m - 2 \gamma \chi_U^2 B^2,$$ (8)

$$b_m(B) = b_m + 4 \gamma M \chi_U B^2,$$ (9)

and the mean field solution for the order parameter is

$$\delta(T_N < T < T_s) \approx -\frac{3}{8b_m(B)} - \frac{a_m}{2b_m(B)T_N}(T_s(B) - T).$$ (10)

For $T_N < T < T_s$ we have $M \approx \chi_U B$ where $\chi_U = \chi - 2\gamma \delta^2 - 2\gamma \chi \delta^4$ is the effective magnetic susceptibility. For $T = T_s(B)$, $\delta^2 \ll 1$ and there is an increase of the susceptibility as $\gamma_2 < 0$. I.e. the magnetization increases as the temperature decreases below $T_s(B)$ in a fixed external magnetic field.

An external magnetic field and the presence of a distortion shift the magnetic transition to lower temperatures:

$$T_N(B) \sim \left(1 - \frac{B^2(c_1 \chi_U^2 + k_1) + 2\gamma_2 \delta^2(T_N)}{a_m} \right)T_N.$$ (11)

The observed reduction of $T_N$ of $\sim 1.5$ K at $B = 16$ T imposes the constraint $a_m \sim c_1 / 5 + 1280k_1$ on the functional parameters.

At the Néel transition, the magnetoelastic coupling produces a kink in $\delta$ due to the onset of $m$. For $T \lesssim T_N$ and $B = 0$ we have

$$\delta(T \lesssim T_N) \sim -\frac{\sqrt{a_m b_m \frac{1}{\delta_s} + 2\gamma \alpha_m \frac{1}{\delta_s} \frac{1}{\delta_s}}}{2b_m b_s - 2\gamma^2}. (12)$$

where we considered the lowest order terms in the coupling and dropped terms of order $c_s/b_s$. Since there is no signature in the specific heat of the structural transition, the jump in the specific heat at the magnetic transition $\Delta C_m \sim a_m^2 T_N / 2b_m$ must be much higher than the corresponding one at the structural $\Delta C_s \sim a_s^2 T_s / 2b_s$ transition. We also require the latent heat at the structural transition $\Delta Q_s \sim \sqrt{\frac{a_m^2}{2b_m}}$ to be small $\Delta Q_s \ll T_N \Delta C_m$. This sets the constrains $a_m^2 / b_m \ll a_m^2 / b_m$ and $c_s \ll a_m b_s / \sqrt{a_M b_m}$ on the parameters. Additionally, we set the parameters to satisfy $m(T \to 0) \sim \sqrt{a_m / 2b_m} \sim 1$ and $\delta(T \to 0) \sim \sqrt{a_m / 2b_m} \sim 0.0005$.

Table 1 lists the parameters used to obtain a qualitative description of the experimental data.

4. Numerical results

Figures 2(a) and (c) present the staggered magnetization $m$ and specific heat $C$ data. The antiferromagnetic transition is shifted towards lower temperatures when the magnetic field is increased as it can be seen in the staggered magnetization $m$ and specific heat $C$ data. The structural order parameter $\delta$ is shown in figure 2(b) as a function of the temperature for different values of the external magnetic field. As the magnetic field increases, the structural transition temperature (where $\delta$ acquires a nonzero value) increases. Note, however, that as a consequence of the $M^2\delta^4$ term in the free energy, the rate of increase of $|\delta|$ decreases as $B$ increases. This term in therefore necessary to explain the behavior of magnetostriiction at low temperatures (see figures 1(e) and 2(e)). The magnetoelastic coupling $\propto \delta^4$ hardens the lattice as the magnetization increases. The qualitative behavior of the experimental data can be accounted including a much larger coupling to the squared magnetization $M^2$ than to the squared staggered magnetization $m^2$. As mentioned above this indicates a non-local magnetoelastic coupling $\propto m_s m_d \delta^4$.

At the Néel transition, $\delta$ presents a kink and a faster absolute value increase for decreasing temperature, as a consequence of the magnetoelastic coupling $\gamma_m m^2 \delta^4$ (with $\gamma_2 < 0$) and the increase of $m^2$ for $T < T_N$. The mean-field solutions for $\delta \delta / dT$ present a divergent behavior $\propto (T_s - T)^{-1/2}$ (see (10) at the structural transition and a discontinuity at the Néel transition (see figure 2(d))). The experimental results, however, are obtained for polycrystalline samples where a distribution of transition temperatures is expected. To take this into account in an approximate way we performed a convolution of the structural order parameter $\delta(T) = (\delta + G)(T)$ with a Gaussian function $G(T)$ of width $\sigma = 1.7$ K$^5$.

Figure 3 presents the numerical results for $\delta$ where, to ease the comparison with the experimental data, the values of $\delta$ are shifted to make them equal to zero at $T = 0$ in figure 3(a), and for $B = 0$ in figure 3(b). The thermal expansion coefficient $\alpha_T = \delta / dT$ presents a broad asymmetric structure at zero field which splits as the magnetic field is increased into a low temperature peak associated with the Néel transition and a high temperature peak due to the structural transition$^6$. Due to

5 We are assuming here the same distribution for the magnetic and the structural transitions.

6 It may seem surprising that the peak associated with the structural transition has a lower height than the one associated with the Néel transition. After the Gaussian convolution, however, the height of the peaks is determined by the area of $d\delta / dT$ near the transition and not by the original height of the peaks.
to the asymmetry of $d\delta/dT$ near the transitions, the peaks in $d\delta/dT$ are shifted to lower temperatures than in the raw data.

The theory describes the main features observed in the experimental data. A large peak is obtained in the specific heat at the magnetic transition and a very small one at the structural transition (see figure 2(c)). The weakness of the latter could explain why it was not observed experimentally as it would fall below the resolution of the experiments in [13].

The Landau theory also reproduces correctly the temperature and magnetic field dependence of the thermal expansion coefficient, including the position and height of the peaks.

As a consistency test of the theory we calculate below the rate of change of the Néel transition with external pressure. On the other hand, from equation (11) we have

$$\frac{dT_N}{dP} \sim -\frac{\beta}{3} \frac{dT_N}{d\delta} = -\frac{2\beta \gamma_2 \delta_{ST}}{3a_m} T_N,$$

(14)

where $\beta \sim 65$ GPa is the bulk modulus (we use here the calculated value for CeScSi reported in [17]), and $\delta_{ST} \sim -3 \times 10^{-4}$ is the dilation at the magnetic transition. This results in $dT_N/dP \sim 1.7$ K GPa$^{-1}$, which is in the same ballpark as the estimated value from Ehrenfest’s relation.

A similar analysis can be done with the magnetic field dependence of $T_N$ using the measured jump of $\partial M/\partial T$ at the transition in a field $B = 1$ T. This results in a good agreement between the model ($\frac{dT_N}{dP} \sim -0.007$ K T$^{-1}$) and the experimental estimations ($\frac{dT_N}{dP} \sim -0.011$ K T$^{-1}$).

Figure 2. (a) Staggered magnetization $m$, (b) structural order parameter $\delta$, (c) specific heat $C$, and (d) linear distortion parameter $d\delta/dT$, as a function of the temperature for different external magnetic fields applied. (e) Structural order parameter and (f) uniform magnetization $M$, as a function of the external magnetic field.
5. Conclusions

We developed a Landau theory to describe phenomenologically the thermal expansion, magnetostriction, magnetization and specific heat data of CeCo_{0.85}Fe_{0.15}Si polycrystalline samples. We find that the available experimental data are compatible with the presence of a structural transition at a temperature \( T_s(B) \) and a magnetic transition at \( T_N(B) < T_s(B) \). The system presents a strong magnetoelastic coupling which leads to an increase in the structural transition temperature with an increasing external magnetic field, and allows the observation of a signature of the magnetic transition in the thermal expansion data. Additional experimental data would be necessary to determine the nature of the structural transition. In particular, it would be important to determine the type of magnetic order and whether the lattice distortion breaks the tetragonal symmetry. A magnetoelastic analysis of additional samples with Fe concentrations \( y < 0.2 \) would allow to determine whether the structural transition temperature \( T_s \) follows the same doping behavior as the specific heat anomaly \( T_A \) which could be associated with the onset of magnetic fluctuations. In the Fe pnictides, the magnetic fluctuations for temperatures \( T \gtrsim T_N \) drive a nematic transition which is concomitant with a structural transition [18–21]. It would be particularly interesting to determine if CeCo_{1−y}Fe_{y}Si compounds have a magnetic and elastic behavior analogous to the one observed in the Fe pnictides. If this is the case, the structural transition would not break the symmetry in the sign of the order parameter \( \delta \) (this can be obtained dropping the \( c_3\delta^3 \) term on (7), which was small in our calculations). An anharmonic elastic coupling between atoms would lead to a change in the volume of the sample given by \( \Delta L/L \propto \delta^2 \) (see e.g. [22]), but would not otherwise change the main conclusion of this work.

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ORCID iDs

William Gabriel Carreras Oropesa https://orcid.org/0000-0001-5210-1151

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