CAN STAR CLUSTER ENVIRONMENT AFFECT DUST INPUT FROM MASSIVE AGB STARS?

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ABSTRACT

We examine the fraction of massive asymptotic giant branch (AGB) stars remaining bound in their parent star clusters (SCs) and the effect of irradiation of these stars by an intracluster ultraviolet (UV) field. We employ a set of N-body models of dynamical evolution of SCs rotating in a galactic potential at the solar galactocentric radius. The cluster models are combined with stellar evolution formulae, a library of stellar spectra, and simple models for SiO photodissociation in the circumstellar environment (CSE). The initial stellar masses of clusters are varied from 50$M_\odot$ to 10$^5M_\odot$. Results derived for individual clusters are combined using a mass distribution function for young SCs. We find that about 30% of massive AGB stars initially born in clusters become members of the field population, while the rest evolve in SCs. They are irradiated by strong intracluster UV radiation, resulting in the decrease of the photodissociation radius of SiO molecules, in many stars down to the dust formation zone. In the absence of dust shielding, the UV photons penetrate in the CSE deeper than 10$R_\odot$ in 64% and deeper than 2$R_\odot$ in 42% of all massive AGB stars. If this suppresses subsequent dust formation, the current injection rate of silicate dust from AGB stars in the local Galaxy decreases from 2.2 $\times$ 10$^{-4}M_\odot$ pc$^{-2}$ Gyr$^{-1}$ to 1.8 $\times$ 10$^{-4}M_\odot$ pc$^{-2}$ Gyr$^{-1}$ at most. A lower revised value of 40% for the expected fraction of presolar silicate grains from massive AGB stars is still too high to explain the non-detection of these grains in meteorites.

Key words: galaxies: star clusters: general – solar neighborhood – stars: AGB and post-AGB – stars: winds, outflows

1. INTRODUCTION

Circumstellar shells of low- and intermediate-mass stars ($0.8M_\odot < M < 8M_\odot$)4 on the thermally pulsing asymptotic giant branch (AGB) are known sites of dust condensation. Some grains from AGB stars, which ended their interstellar journey as material forming the solar system 4.6 Gyr ago, have been preserved in meteorites. The presolar origin of these grains (initial masses and metallicities of their parent stars) can be ascertained from anomalous isotopic ratios of the major and many trace elements characterizing stellar nucleosynthesis (Hoppe & Zinner 2000; Nittler 2003; Dorschner 2010; Zinner 2014).

Silicates and oxide grains are condensed in oxygen-rich stellar winds of AGB stars. The third dredge-up process mixes the carbon-rich ashes from He nuclear burning into the convective envelope, turning a star into a carbon star. This process becomes more efficient with increasing stellar mass, therefore only low-mass AGB stars in the mass range 1–1.5 $M_\odot$ are prominent sources of oxygen-rich dust. However, massive AGB stars with initial mass from 3.5–5 $M_\odot$ up to 8 $M_\odot$, depending on model details and metallicity (Busso et al. 1999; Marigo 2007), convert the dredged-up carbon into $^{13}$C as a result of the hot-bottom burning process. There is recent spectroscopic evidence that hot-bottom burning is active from the first thermal pulses through their final superwind phase (Justtanont et al. 2012; Garcia-Hernandez et al. 2013).

Theoretical models of dust condensation in stellar winds of evolved stars indicate that massive AGB stars should produce significant amount of oxygen-rich dust (e.g., Ferrarotti & Gail 2006; Gail 2010; Ventura et al. 2012; Nanni et al. 2013). Models of the lifecycle of grains of different origins show that the oxygen-rich grains from massive AGB stars are expected to be an abundant component of the presolar grain population comparable to that from low-mass stars (Gail et al. 2009). The fact that grains are efficiently condensed in shells of AGB stars experiencing hot-bottom burning is supported by spectroscopic observations of oxygen-rich dust-enshrouded stars (e.g., van Loon et al. 2005a). The chemical composition of these stars is altered by the hot-bottom burning process, leading to subsolar values of $^{12}$C/$^{13}$C and $^{16}$O/$^{18}$O isotope ratios (Boothroyd et al. 1995), which should be possible to detect in presolar grains. However, no oxygen-rich grain with signatures of hot-bottom burning has been conclusively identified in meteorites so far. The entire population of presolar oxygen-rich grains appears to originate from low-mass AGB stars (Iliadis et al. 2008; Nittler et al. 2008; Vollmer et al. 2008; Nittler 2009; Hoppe 2010; Palmerini et al. 2011). To shed light on the origin of this discrepancy between theoretical models and findings from presolar grain studies, we consider additional processes that can potentially reduce the global dust input from intermediate-mass stars.

The total contribution of massive AGB stars to the Galactic dust budget depends on the adopted dust yields, i.e., on the amount of dust condensed in the stellar wind over the whole AGB evolution of a star. Dust yields as a function of the initial stellar mass and metallicity have been derived over the past decade from extensive calculations combining evolution of AGB stars, stellar wind and dust condensation models (e.g., Ferrarotti & Gail 2006; Ventura et al. 2012; Nanni et al. 2013). Such models consider single isolated AGB stars under standard interstellar conditions. Nucleation and growth of dust particles in outflows of these stars is assumed to be independent of their

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4 We do not consider super-AGB stars and assume that the upper limit is determined by the maximum mass of stars that develop an electron-degenerate CO core and end their life as white dwarfs (but see Doherty et al. 2013).
environment. This is justified for the irradiation of the circumstellar environment (CSE) by the standard interstellar radiation field (ISRF), because the dust formation zone is located much deeper in the shell than the photodissociation region (e.g., Jura & Morris 1981; Glassgold et al. 1987; Mamon et al. 1987; Glassgold 1996). This may not be the case for evolved stars in young star clusters (SCs). Unlike low-mass stars, intermediate-mass stars are more likely to be members of their parent SCs during their AGB evolution.

The majority of stars in the mass range $4M_\odot < M < 8M_\odot$ are formed in massive SCs, which survive cloud dispersal and become open clusters, as will be shown below. The dissolution of SCs is a result of the photodissociation of SiO molecules that occurs in the circumstellar shells of massive AGB stars, as discussed in Pelupessy & Portegies Zwart (2012) and Baumgardt & Kroupa (2008). The CSE of massive AGB stars in young SCs is subject to irradiation by the intracluster ultraviolet (UV) field from main sequence cluster stars of spectral types B and early A. Strong UV irradiation of CSE may affect the dust condensation process. Beck et al. (1992) investigated dust condensation in stellar winds of stars with ionizing radiation of chromospheric origin and found that UV photons are able to reduce and, for certain field strengths, completely suppress the nucleation process. If the amount of dust condensed in outflows of massive AGB stars in SCs is affected by external UV radiation, the net dust input from these stars will be reduced.

In order to assess the importance of cluster environment to the CSE of massive AGB stars, first of all we need to estimate the fraction of intermediate stars in the local Galaxy that evolve in their parent SCs. To this end, we employ numerical simulations of the dynamical evolution of SCs in a mass range of $50-10^3 M_\odot$ coupled with stellar evolution prescriptions (Just et al. 2009; Kharchenko et al. 2009; Ernst et al. 2010). Next, for the massive AGB stars that remain bound in the cluster, we calculate the UV radiation field created by the neighboring main sequence cluster members as a function of cluster mass. For a simple estimate of the impact of the intracluster radiation field on the circumstellar shells of AGB stars in a cluster, we consider photodissociation of the SiO molecule. The SiO molecules are the basic building blocks for silicates, the most widespread dust species in oxygen-rich environments (Hening 2010; Gail & Sedlmayr 2014). They are formed in the stellar photosphere, and in the shell their abundance decreases due to two processes: depletion on grains in the dust condensation zone and then photodissociation caused by interstellar UV photons in the outer regions. We calculate the photodissociation radius of the SiO molecule for each massive AGB star in the model clusters and compare these radii to the position of the dust formation zone.

The structure of our paper is as follows. Section 2 describes a suite of dynamical models of SC evolution, size–frequency distribution of SCs, and our main assumptions in calculations of the UV fluxes irradiating circumstellar shells of massive AGB stars. Results of model calculations of dynamical evolution of model SCs are presented in Section 3. We show that about 70% of massive AGB stars initially born in clusters remain cluster members. For these stars, we investigate the location of the photodissociation radii of SiO molecules with respect to the dust formation zone in their CSE. The dependence of our main results on the initial mass–radius relation for SCs is presented in Section 4. Discussion and concluding remarks are given in Section 5.

2. MODEL

2.1. Simulations of SC Evolution

The dynamical evolution of SCs is modeled as pure N-body systems of gravitationally bound stars rotating in a galactic potential at the solar galactocentric radius of 8.5 kpc. The simulations were carried out with the direct N-body code GRAPE (Harfst et al. 2007) on high-performance computing clusters with accelerator hardware GRAPE or GPU selected by appropriate libraries. These models were introduced and applied to individual SCs in a series of papers (Just et al. 2009; Kharchenko et al. 2009; Ernst et al. 2010). In the following, we briefly summarize the main model parameters used in our calculations and refer to the original publications for a detailed description.

2.1.1. Initial Mass–Radius Relation

We consider the evolution of low- and intermediate-mass stars in clusters, after the last massive stars ended their life as supernovae, corresponding to the cluster ages of 40 Myr. Initially SCs are embedded in their parent molecular clouds, which are completely cleared away by stellar feedback by the onset of our simulations. Modeling of the evolution of embedded clusters and their emergence from parent molecular clouds requires the inclusion of gas dynamics or special algorithms accounting for the influence of gas on stellar dynamics as discussed in Pelupessy & Portegies Zwart (2012) and Baumgardt & Kroupa (2007). These authors showed that the dynamical friction drives early mass segregation, resulting in preferential retention of stars with mass above $2M_\odot$ in clusters. Therefore we neglect possible ejection of stars during the early cluster evolution before the onset of our simulations.

For the initial distribution of stars in the clusters, we adopt commonly used non-rotated King models (King 1966) with a central potential of $W_0 = 6.0$ (Einsel & Spurzem 1999). In this case, the initial mass distribution is given by three parameters: the initial cluster mass, concentration parameter, and scale radius. Observed shapes of SCs as well as their sizes for a given cluster mass vary in a large range and can poorly constrain the initial conditions for simulations (Larsen 2004; Portegies Zwart et al. 2010). This is due to the fact that they are influenced by a number of physical processes such as cluster formation, internal processes (self-gravitation, binary fraction, rotation), external forces (tidal field of the galaxy), and encounters with giant molecular clouds (Scheepmaker et al. 2007; Piskunov et al. 2008b; Kharchenko et al. 2009). The importance of these processes for the initial conditions of SC models is reviewed by Kroupa (2008). To minimize the number of free parameters, we adopt a relation between the initial mass and radius

$$R_{cl} \approx 50 \sqrt{M_{cl}/10^5 M_\odot} \, \text{(pc)}$$

derived from observations of molecular clouds and clumps in the Milky Way (Larson 1981; Rivolo & Solomon 1988). This mass–radius relation has been used to set up the initial conditions for simulations of open clusters in the Milky Way (Adams et al. 2006; Fatuzzo & Adams 2008; Kharchenko et al. 2009). It has also been applied in theoretical studies of tidal tail clumps of SCs (Just et al. 2009) and for calibration of radii and masses of observed clusters with simulations (Ernst et al. 2010). The initial half-mass radius of each cluster was adjusted so that the half-mass radius of a King model was...
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Table 1
InitialParametersoftheN-bodyModels

| Nₜ | Nₜₐm | Mₐ₁ (M☉) | Rₜtidal (MRR) (pc) | Rₜtidal (TRR) (pc) | N₁ₕₐ₁/Mₜₐ₁≤ₘₜₐ₁≤ₘₙ (| N₂ₜₐ₁/Mₜₐ₁≤ₘₜₐ₁≤ₘₙ (| N₂ₜₐ₁/Mₜₐ₁≤ₘₜₐ₁≤ₘₙ |
|-----|------|----------|-------------------|-------------------|------------------|------------------|
| 109 | 4    | 50       | 0.25              | 0.75              | 1, 2, 1, 1       | 3, 3, 4, 5       |
| 153 | 4    | 70       | 0.35              | 0.84              | 1, 2, 2, 2       | 5, 5, 6, 6       |
| 218 | 4    | 10²      | 0.44              | 0.95              | 1, 2, 2, 2       | 7, 4, 7, 8       |
| 437 | 4    | 2 × 10³  | 0.54              | 1.20              | 3, 2, 5, 5       | 15, 9, 17, 15   |
| 1094| 4    | 5 × 10²  | 0.85              | 1.63              | 11, 12, 10, 9    | 30, 28, 40, 27  |
| 1532| 4    | 7 × 10²  | 1.04              | 1.82              | 16, 21, 13, 12   | 50, 51, 47, 54  |
| 2189| 4    | 10³      | 1.29              | 2.05              | 19, 25, 21, 23   | 60, 69, 66, 77  |
| 4379| 4    | 2 × 10³  | 1.81              | 2.58              | 36, 49, 48, 46   | 130, 155, 140, 142 |
| 10947| 4   | 5 × 10³  | 2.85              | 3.50              | 100, 118, 105, 111 | 364, 373, 345, 351 |
| 15326| 4   | 7 × 10³  | 3.30              | 3.92              | 164, 132, 142, 149 | 519, 510, 492, 492  |
| 21895| 1   | 10⁶      | 3.99              | 4.41              | 203              | 716              |
| 43791| 1   | 2 × 10⁶  | 5.69              | 5.56              | 415              | 1454             |
| 109476| 1  | 5 × 10⁶  | 8.96              | 7.55              | 1025             | 3620             |
| 153268| 1  | 7 × 10⁶  | 10.62             | 8.44              | 1482             | 5096             |
| 218955| 1  | 10⁷      | 12.66             | 9.51              | 2059             | 7272             |

Notes. The columns give first the total number of stars, followed by the number of simulation runs, the initial cluster mass, the initial half-mass radius for the mass–radius relation and that for the tidal radius–mass relation. The last two columns give the number of massive AGB stars and the number of irradiating stars in each simulation.

Initially equal to 80% of a scaling radius. We refer to models with the initial mass–radius relation given by Equation (1) as MRR models.

Given that there are no strong observational constraints or a universal relation for the initial conditions of simulated clusters, we test the dependence of our results on the adopted initial mass–radius relation and perform two different sets of simulations. We follow an alternative method to set up the initial conditions, assuming that the initial cluster radius is determined by the tidal field of the Galaxy and is given by (Innanen et al. 1983; Baumgardt & Makino 2003; Lamers et al. 2013)

$$R_{\text{tidal}} = \left(\frac{0.5GM_{\text{cl}}}{V_G^2}\right)^{\frac{1}{3}}R_G^{2/3},$$

where $M_{\text{cl}}$ is the cluster mass, $R_G$ the galactocentric distance of the cluster, and $V_G$ the circular velocity of the Galaxy. This set of models is denoted as TRR. The half-mass radii for TRR and MRR models are shown in Table 1.

Additionally, we perform a simulation run with the constant initial radius for all clusters (CRR models) to include the case of a weak mass–radius relation suggested by some observations of galactic and extragalactic SCs (Larsen 2004; Scheepmaker et al. 2007). We adopt a value of the initial half-mass radius of 2 pc consistent with the range of values from observations (Lamers et al. 2013). In the following, we use the MRR models as the reference models and refer to them in the analysis of the results, unless stated otherwise. Comparison of the main results for the TRR and CRR models with the reference models is given in Section 4.

2.1.2. Stellar Mass Distribution in SCs

The stellar mass in clusters is distributed following the initial mass function (IMF) from Kroupa (2002) where only stars in the mass range $0.08 \leq m \leq 8.0$ $M_\odot$ are considered. Stellar evolution of stars in clusters (stellar luminosities, radii, effective temperatures at various evolutionary phases) is described according to the analytical formulas from Hurley et al. (2000). Binaries as well as multiple star systems are not included in our study. Possible encounters of SCs with giant molecular clouds as well as passages of spiral arm or disk shocking were neglected.

The initial mutual distribution of stars of different mass in clusters is still debated. There are many observational studies in support of the initial mass segregation (IMS) of stellar mass, i.e., concentration of more massive stars in the inner cluster region (see Lada & Lada 2003; Portegies Zwart et al. 2010, and references therein). However, observational evidence of mass segregation was questioned by Ascenso et al. (2009), who pointed at difficulties in differentiating between segregation and sample incompleteness effects. There are observations that indicate that very low-mass stars associated with a cluster are distributed homogeneously in a volume that is much larger than the core of a cluster (Kumar & Schmeja 2007). Given these uncertainties in the initial mass distribution in SCs, we run two sets of models: with and without IMS to study how it affects the evolution of massive AGB stars. Initial conditions for clusters with segregation are derived accordingly to the procedure described by Baumgardt et al. (2008). It invokes a random number generator to draw distributions of initial stellar masses, positions, and velocities of stars in clusters.

2.1.3. Initial Parameters of Model Clusters

We consider the dynamical evolution of 15 clusters with and without IMS, resulting in 30 set-ups of simulation models. Initial masses, radii, and numbers of stars for each cluster are listed in Table 1. All clusters are moving on circular orbits in the Galaxy represented by an analytic background potential described by Plummer–Kuzmin models (Miyamoto & Nagai 1975) with circular velocity $V_G = 233$ km s$^{-1}$. Model SCs are assumed to have solar metallicity. For small clusters, the number of stars within a given mass range depends on randomized discretization of the initial stellar mass over individual stars. Therefore, we generate several sets of initial conditions for SCs with initial masses $M_{\text{cl}} \leq 7 \times 10^3 M_\odot$, resulting in 90 simulation models in total for one set. The number of simulation runs for each cluster model is given in the second column of Table 1. The table also shows the total
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numbers of stars with mass \( m \geq 4M_\odot \), which experience hot-bottom burning during TP-AGB evolution, and with \( m \geq 2M_\odot \), which dominate the intracluster UV radiation field, in each simulation run. According to Weidner et al. (2013) (see also Kroupa et al. 2013, pp. 115–242) the lowest mass of a SC to host at least one massive TP-AGB star is \( \sim 50M_\odot \). Therefore this value is adopted here for \( M_{\text{cl}}^\text{min} \). We adopt an upper mass limit of model clusters \( M_{\text{cl}}^\text{max} = 10^5M_\odot \), appropriate for the Milky Way (Kruĳssen 2014, and references therein). SCs of higher mass in the Galaxy belong to metal-poor, \( \geq 10 \) Gyr old globular cluster systems. Given short lifetimes of grains in the ISM (Slavin et al. 2015), dust from massive AGB stars from globular clusters could not survive until the formation of the solar system and is excluded from our consideration.

Relevant information about all stars from the simulation runs (e.g., their coordinates, masses, luminosities, temperatures) is stored in snapshots with a time step of \( \sim 0.1 \) Myr. It is thus ensured that each massive TP-AGB star appears in several snapshots.

### 2.2. Fraction of Massive AGB Stars in Clusters

In order to combine the results derived for individual SCs of different masses to estimate the total fraction of massive AGB stars evolving in clusters, we need to know the cluster mass distribution function for the onset of simulations corresponding to the cluster age of 40 Myr. We assume that most of stars are formed in clusters embedded within giant molecular clouds (Lada & Lada 2003; but see also Kruĳssen 2012; Adamo et al. 2015). The distribution function of embedded SCs can be measured observationally by infrared star counts. However, only the most massive \( (M_{\text{cl}} > 500M_\odot) \) embedded clusters survive and become stable, open clusters (Lada & Lada 2003; Bonatto & Bica 2011). Since by the age of 40 Myr all clusters should emerge from their birth places, we can adopt the mass distribution function of embedded SCs, with a correction for the infant mortality of low-mass SCs as described below.

#### 2.2.1. Embedded SC Mass Function

Observations indicate that the mass–frequency distribution of young embedded SCs \( dn_{\text{emb}}(M_{\text{cl}})/dM_{\text{cl}} \) follows a universal power law (e.g., Kennicutt et al. 1989; McKee & Williams 1997; Lada & Lada 2003; Larsen 2010; Portegies Zwart et al. 2010):

\[
dn_{\text{emb}}(M_{\text{cl}})/dM_{\text{cl}} \propto M_{\text{cl}}^{-2}, \quad M_{\text{cl}}^\text{min} \leq M_{\text{cl}} \leq M_{\text{cl}}^\text{max},
\]

where \( dn_{\text{emb}}(N_{\text{cl}}) \) is the number of embedded SCs with masses between \( M_{\text{cl}} \) and \( M_{\text{cl}} + dM_{\text{cl}} \); \( M_{\text{cl}}^\text{min} \) and \( M_{\text{cl}}^\text{max} \) are the lowest and highest SC masses. As discussed above, we assume \( M_{\text{cl}}^\text{min} = 50M_\odot \) and \( M_{\text{cl}}^\text{max} = 10^5M_\odot \), respectively.

The total number of AGB stars formed in all clusters with masses below \( M_{\text{cl}} \) is

\[
N_{\text{AGB}}^\text{tot}(M_{\text{cl}}) = \int_{M_{\text{cl}}^\text{min}}^{M_{\text{cl}}^\text{max}} N_{\text{AGB}}(M) \frac{dn_{\text{emb}}(M)}{dM} dM,
\]

where \( N_{\text{AGB}}(M) \) is the initial number of AGB stars in a cluster with mass \( M \).

The cumulative number of AGB stars formed in a cluster with mass \( M < M_{\text{cl}} \) normalized to the total number of these stars is easily derived from Equation (4):

\[
f_{\text{AGB}}^{\text{cum}}(M_{\text{cl}}) = \int_{M_{\text{cl}}^\text{min}}^{M_{\text{cl}}} N_{\text{AGB}}(M) \frac{dn_{\text{emb}}(M)}{dM} dM \int_{M_{\text{cl}}^\text{min}}^{M_{\text{cl}}^\text{max}} N_{\text{AGB}}(M) \frac{dn_{\text{emb}}(M)}{dM} dM.
\]

Figure 1 shows the cumulative distribution of stars with initial masses \( 4M_\odot < M < 8M_\odot \), which are progenitors of massive TP-AGB stars, as a function of initial cluster mass for the distribution function of young clusters given by Equation (3). It is derived for the adopted Kroupa IMF and cluster mass range.

Because of gradual dissolution of SCs, the actual values of bound AGB stars \( N_{\text{AGB}}(M_{\text{cl}}) \) derived from simulations are lower. Additionally, the mass distribution function of embedded SCs has to be corrected for the dissolution of low-mass clusters upon dispersal of molecular clouds as described below.

#### 2.2.2. Dissolution of Low-mass Clusters

Numerical models in this work consider evolution of clusters shortly after emergence from molecular clouds, therefore we include two sources of the field population of massive AGB stars separately: (i) members of low-mass clusters \( (M_{\text{cl}} < 500M_\odot) \) that did not survive dispersal of molecular clouds, and (ii) stars lost by bound clusters in the process of their dynamical evolution. The latter is derived from our dynamical N-body models as a function of initial cluster mass.

The fraction of SCs that survive as bound systems up to Pleiades age was assessed by Lada & Lada (2003) by comparison of the numbers of embedded and open SCs from observations. They found that majority (90%–95%) of embedded SCs with initial mass \( M_{\text{cl}} \lesssim 500M_\odot \) emerge from molecular clouds as unbound systems and contribute their members to the field population. The contribution of clusters in...
this mass range to the total number of progenitors of massive TP-AGB stars is about 30%, while about half of progenitors of massive AGB stars are formed in clusters with mass above $2 \times 10^3 M_\odot$ (Figure 1).

Dynamical models that consider embedded evolution of SCs in molecular clouds find that the survival of embedded SCs depends on many physical parameters such as gas expulsion timescale, star formation efficiency, and impact of an external tidal field (Parmentier 2011; Parmentier & Baumgardt 2012). Nevertheless, the slopes of the mass functions of embedded or young SCs and gas-free clusters are identical (Lada & Lada 2003; Oey et al. 2004; Dowell et al. 2008). For a simple estimate of the contribution of clusters $M_\text{cl} \lesssim 500 M_\odot$ to the field population, we assume that initially these SCs were formed according to the mass distribution function $dn_{\text{emb}}(M)/dM$ given by Equation (3) like their higher mass counterparts, but 90% of these clusters do not survive cloud dispersal based on the lower limit derived by Lada & Lada (2003) and more recently by Bonatto & Bica (2011). Therefore, for the onset of our simulation, we adopt the mass distribution function of young SCs $dn_{\text{con}}(M)/dM$ corrected for the dissolution of low-mass clusters by multiplication of $dn_{\text{emb}}(M)/dM$ by 0.1 for $M_\text{cl} \lesssim 500 M_\odot$.

The total number of bound AGB stars is given by

$$N_{\text{AGB}}^{\text{bound}} = \int_{M_{\text{cl}}}^{M_{\text{cl}}^\text{max}} N_{\text{AGB}}^b(M) \frac{dn_{\text{con}}(M)}{dM} dM$$

where $N_{\text{AGB}}^b(M)$ is the number of bound stars in a SC with mass $M$ derived from numerical simulations of dynamical SC evolution. The total number of bound AGB stars residing in SCs with $M < M_\text{cl}$ relative to the number of all AGB stars is therefore given by

$$f_{\text{AGB}}^{\text{cum}}(M_\text{cl}) = \frac{1}{N_{\text{AGB}}^{\text{tot}}} \int_{M_{\text{cl}}}^{M_{\text{cl}}^\text{max}} N_{\text{AGB}}^b(M) \frac{dn_{\text{con}}(M)}{dM} dM,$$

where $N_{\text{AGB}}^{\text{tot}}$ is given by Equation (4) for $M_\text{cl} = M_{\text{cl}}^\text{max}$.

### 2.3. Intracluster UV Radiation Field

Circumstellar envelopes of evolved stars in young SCs are irradiated by UV radiation emitted by the main sequence cluster members of spectral types A and late B. In older clusters, thermal radiation from white dwarfs becomes an important source of UV photons, which is probably responsible for the ionization and removal of intracluster medium (McDonald & Zijlstra 2015). The strength of the intracluster UV radiation field due to main sequence stars is expected to quickly decrease over a few hundred Myr as the cluster turn-off point shifts toward stars of lower mass, since the amount of emitted UV radiation is a strong function of stellar mass. It is illustrated in Figure 2, showing the total number of ionizing photons for H I and C I atoms emitted per unit time $Q_0$ as a function of initial mass for intermediate-mass stars. $Q_0$ is derived by integration of the stellar surface flux $F_\nu$:

$$Q_0 = \int_{\nu_{\text{min}}}^{\nu_{\text{max}}} \frac{4\pi R_\star^2 F_\nu}{h\nu} d\nu,$$

where $R_\star$ is the stellar radius, and $\nu_{\text{max}}$ and $\nu_{\text{min}}$ correspond to the wavelengths of 91.178 and 240 nm (5.17 eV) for H I and to 91.178 and 110.11 nm (11.26 eV) for C I, respectively.

Intermediate-mass main sequence stars in clusters are capable of ionizing the intracluster medium. Their radiation is hardly attenuated within the cluster owing to the observed lack of gas and dust in the intracluster medium (Bastian & Strader 2014). Figure 2 shows the radii of Strömgren spheres, i.e., zones of ionized H II and C II around the central star, for the homogeneous intracluster gas density of 1 cm$^{-3}$, similar to the density of the ambient ISM. Although the sizes of ionized regions around intermediate-mass stars are small compared to those around massive stars, they are comparable to the sizes of low-mass clusters (Table 1). After the onset of mass loss from evolved stars in clusters, the density distribution in the vicinity of these stars will follow an $r^{-2}$ radial dependence and only outer layers will be ionized by the extreme UV radiation.

The strength of the UV field is customarily characterized relative to the standard ISRF (Röllig et al. 2007):

$$\chi = \int_{\nu_{\text{91.2 nm}}}^{\nu_{\text{240 nm}}} \lambda \Omega_{\text{ISRF}} \nu^2 d\nu / \int_{\nu_{\text{91.2 nm}}}^{\nu_{\text{240 nm}}} \lambda \nu \Omega_{\text{ISRF}} \nu d\nu,$$

where $\Omega_{\text{ISRF}} = 4\pi c / \nu^2$ is the spectral photon energy density and $\nu_{\text{ISRF}}$ is the spectral photon energy density of the ISRF (Draine 1978). The mean radiation field intensity in the location of an AGB star is approximated as

$$4\pi J_{\nu} = \sum_{i=1}^{n_{\text{MS}}} \Omega_{\nu}^{\text{int}} I_{\nu}^{\text{sd}} + 4\pi J_{\text{ISRF}} = \sum_{i=1}^{n_{\text{MS}}} \frac{R_i^2}{r_i^2} I_{\nu}^{\text{sd}} + 4\pi J_{\text{ISRF}},$$

where $n_{\text{MS}}$ is the current number of main sequence stars with $m_* > 2 M_\odot$ in a cluster, $I_{\nu}^{\text{sd}}$ is the incident intensity from the th star, $R_i$ is its photospheric radius, $r_i$ is the distance from the central AGB star to the th star, and $\Omega_{\nu}^{\text{int}}$ is the solid angle subtended from the th star. The last term on the right side of the equation is the contribution from the ISRF. $I_{\nu}^{\text{sd}}$ is derived from the Eddington fluxes $H_\nu$ provided by a stellar spectral library,$^a$

$$I_{\nu} = \frac{F_{\nu}}{\pi} = \frac{4c}{\nu^2} H_\nu.$$

The stellar fluxes are assigned to cluster stars according to their temperature and surface gravity stored in the snapshots. We employ the BaSeL 3.01 semi-empirical library of stellar spectra.
for wavelengths from 9 nm to 160 µm (Lejeune et al. 1997, 1998; Westera et al. 2002).

2.4. Photodissociation Radius of SiO Molecules

The SiO molecule is considered a prerequisite for formation of quartz and grains of various silicate types (Henning 2010; Gail & Sedlmayr 2014). It is well established by photochemical models and supported by observations that the SiO molecules decreases with radius in the CSE of AGB stars by two processes: depletion on grains in the dust condensation zone and dissociation by interstellar UV photons in outer regions (Jura & Morris 1981; Huggins & Glassgold 1982a, 1982b; González Delgado et al. 2003). Such photochemical models usually assume a homogeneous dust distribution with dust attenuation properties similar to those in the interstellar medium. In this case, dust shielding plays a crucial role in the chemistry of CSE, being able to protect molecules from the interstellar UV photons up to distances of $10^{16}$–$10^{17}$ cm (Glassgold 1996). In this work, we evaluate how deep the UV photons can penetrate in the expanding shell of an AGB star, which is irradiated by the enhanced UV radiation prior to the onset of efficient dust condensation. We consider the sizes of the SiO envelopes around AGB stars in the model clusters and compare them to those irradiated by the ambient ISRF, and to the position of the dust formation zone.

For a rough estimate, we adopt a toy model of the photodissociation of an SiO molecule in a stationary spherically symmetric outflow, where the gas has been accelerated to terminal velocity $v_t$. In the absence of other sinks and sources, the SiO fractional abundance $f_{\text{SiO}}$ relative to H$_2$ changes due to photodissociation by UV photons as (Jura & Morris 1981; Huggins & Glassgold 1982b)

$$
\frac{df_{\text{SiO}}}{dr} = -\frac{k_{\text{SiO}}^{\text{pd}}}{v_t} \exp\left(-\frac{d_{\text{SiO}}}{r}\right)
$$

where $d_{\text{SiO}}$ is the shielding distance corresponding to the optical depth of 1 and $k_{\text{SiO}}^{\text{pd}}$ is the unattenuated photodissociation rate of SiO molecules. For a monosized grain distribution, the shielding distance is

$$
d_{\text{SiO}} = 1.4 \left(\frac{Q}{\rho_{\text{SiO}}}\right) a_{\text{SiO}} \times \frac{M_d}{4\pi v_t},
$$

where $Q$ is the dust absorption efficiency, $a$ is the grain size, $\rho_{\text{SiO}}$ is the density of the solid material, and $M_d$ is the dust mass-loss rate. The grain drift relative to the gas was neglected. The value of dust mass loss is $M_d = DM$, where $D$ is the dust-to-gas ratio in the stellar wind and $M$ is the gas mass-loss rate from Equation (16).

The size of the SiO envelopes derived from observations agrees well with the photodissociation radius defined as the distance from the central star where the SiO abundance is decreased by $e$ times (González Delgado et al. 2003). The equation for the photodissociation radius is derived from Equation (12) (Jura & Morris 1981)

$$
r_p = \frac{v_t}{k_{\text{SiO}}^{\text{pd}} E_2(d_{\text{SiO}}/r_p)},
$$

where $E_2(x)$ denotes the exponential integral. Equation (14) is solved numerically for all AGB stars in the model clusters. In the dust-free case, the photodissociation radius is simply given by

$$
r_p = v_t/k_{\text{SiO}}^{\text{pd}}.
$$

The unattenuated photodissociation rate of SiO molecules through line absorption from the lower level $l$ into an upper state level $u$ is (van Dishoeck et al. 2006)

$$
k_{\text{SiO}}^{\text{pd}} = \pi e^2 m_e c f_{\text{sd}} \eta_u \frac{4\pi l_u(v_{ul})}{h v_{ul}},
$$

where $f_{\text{sd}}$ is the line absorption oscillator strength and $\eta_u$ is the dissociation efficiency of the upper state $u$, which lies between 0 and 1. Assumption of $\eta_u = 1$ is reasonable for SiO molecules. Mutual shielding and self-shielding are the factors that can reduce the photodissociation rate of such molecules as CO and H$_2$. Mutual shielding is probably not important for SiO (E. van Dishoeck 2015, private communication). The total photodissociation rate is computed by summing over all lines. We include absorption to the $3 \Sigma^+$ and 2, 3, 4, and 5 $\Pi$ states for SiO molecule with the oscillator strength $f = 0.10, 0.32, 0.03, 0.11$, and 0.10, respectively, taken from the photodissociation database$^5$ (van Dishoeck et al. 2006). The wavelengths for absorption lines are 1011, 1058, 1063, 1140, and 1378 Å.

The mean intensity $J_u$ is derived from Equation (10) for the intracorona radiation field, and is taken from work by Mathis et al. (1983) for the ISRF.

2.4.1. Wind Model Parameters

We focus on dust formation by massive AGB stars with hot-bottom burning, therefore we consider only an oxygen-rich dust mixture in circumstellar envelopes. Although the dust composition in envelopes of M-stars depends on the initial stellar mass and mass-loss rates, for simplicity we assume a fixed silicate composition with density $\rho_d = 3.3$ g cm$^{-3}$. We adopt the following values of the dust-to-gas ratio $D$ in the wind: $D = 0$ corresponding to a dust-free case, and $D = 0.001$, a typical value in outflows after the condensation zone derived from theoretical models of massive AGB stars. Grains are assumed to have a single size of 50 nm. The absorption efficiency $Q$ for a grain size of $a = 50$ nm and $\lambda = 100$ nm equates to 1. The optical depth at around 100 nm, calculated for the adopted grain size, is half that calculated for a power-law distribution of grain sizes from work by Kim et al. (1994), which is commonly assumed in spectral energy distribution fitting.

The mass-loss rate is assumed to be isotropic. We adopt the mass-loss rate for oxygen-rich AGB stars derived empirically by van Loon et al. (2005a), which is more suitable for massive AGB stars than Reimer’s law:

$$
M = 1.38 \times 10^{-11} \left(\frac{L}{L_\odot}\right)^{1.05} \left(\frac{T_{\text{eff}}}{3500 \text{ K}}\right)^{-6.03},
$$

where $L$ and $T_{\text{eff}}$ are the luminosity and effective temperatures of TP-AGB stars. The expansion velocity $v_t$ is assumed to be 10 km s$^{-1}$. For Si abundance, the value $c_{\text{Si}} = 4 \times 10^{-5}$ is adopted. It is assumed that initially all Si atoms are bound in SiO molecules.

$^5$ http://home.strw.leidenuniv.nl/~ewine/photo/
3. RESULTS

In this section, we present results of model evolution of massive AGB stars in SCs of various initial mass (Table 1) rotating in the Galaxy at the solar galactocentric radius from simulation time \( t = 40 \) Myr up to 220 Myr corresponding to the lifetimes of these stars.

3.1. The Fraction of Massive AGB Stars in Clusters

The relative fractions of bound and unbound massive AGB stars for each model cluster are displayed in Figure 3. The fraction is derived from the analysis of binding energies of all massive AGB stars in the cluster for the entire simulation run. Most unbound massive AGB stars originate from low-mass SCs. While low-mass clusters with IMS eject a slightly higher number of massive AGB stars compared to the models without IMS, it is the opposite for massive clusters \((M_d > 2 \times 10^3M_☉)\), with IMS which keep almost all their massive AGB stars. The fractions of massive AGB stars lost by massive clusters modeled without IMS are 0.2%–6%.

Figure 4 shows the cumulative distribution of massive AGB stars calculated with the mass distribution function of SCs as described in Section 2.2. Most unbound progenitors of massive AGB stars that eventually become members of the field population originate from SCs with low mass, while more massive clusters preserve their massive AGB stars (see Figure 3). The majority of low-mass clusters are dissolved in the process of emergence from their parent molecular clouds before the onset of our simulations. This is taken into account in the same way for both types of initial conditions, therefore the cumulative distributions derived for models with and without IMS appear very similar in Figure 4. Our main finding is that 70% of massive AGB stars at the solar galactocentric radius reside in SCs. 30% of all massive AGB stars were lost from their clusters prior to the onset of AGB evolution and evolve in the field. They originate mainly from SCs with initial mass \( M_d < 10^3M_☉\). In the following we focus on massive AGB stars in a cluster environment and its effects on their circumstellar envelopes.

3.2. Intracluster UV Radiation Field

Figures 5–7 show the strength of the unattenuated intracluster radiation field at the locations of massive AGB stars for SCs with initial mass \( M_d = 10^2, 10^3, 10^4, \) and \( 10^5M_☉\). The intracluster radiation field is calculated for each snapshot by summing up the fluxes of photons in the energy range 5.6–13.598 eV from all cluster main sequence stars with mass \( m \geq 2M_☉\). In order to compare the irradiation that an AGB star experiences in a SC to that in the ISM, the fluxes are shown relative to the standard ISRF. We adopt the value of the photon flux \( F_{\text{Draine}} = 1.921 \times 10^8 \text{cm}^{-2} \text{s}^{-1} \) (Draine 1978).

Since the duration of the thermally pulsing AGB stage is relatively short, low-mass clusters have no more than one star in this evolutionary phase at the same time (Figure 5). A cluster with \( M_d = 10^4M_☉\) has up to four TP-AGB stars at the same time, while a \( 10^5M_☉\) cluster has generally more than four massive AGB stars. The UV fluxes at the location of multiple AGB stars are shown with different symbols depending on their number in Figures 6 and 7.

Although there is a scatter in the values of the UV flux, Figures 5 and 6 demonstrate that most AGB stars are irradiated by a 10–100 times stronger UV field than the ISRF. The average irradiation flux decreases with time as stars of higher mass go off the main sequence (Figure 2). There is a spread of more than an order of magnitude in UV flux strength toward lower values for clusters without IMS resulting from their more extended stellar distribution.

3.3. Photodissociation of SiO Molecules by Intracluster Field

3.3.1. Photodissociation Radii of SiO Molecules in Cluster AGB Stars

We compute the photodissociation radii \( R_{\text{pd, SiO}} \) of SiO envelopes of bound AGB stars in all simulated clusters for two cases of UV irradiation: (i) by the intracluster radiation field at the location of each AGB star in model clusters, and (ii) by the standard isotropic ISRF, for comparison. Figure 8 shows the photodissociation radii for cluster masses of \( 10^2, 10^3, \) and \( 10^5M_☉\) for MRR models with and without IMS for a dust-free stellar wind. This case corresponds to the onset of the dust condensation process. Time variations of the photodissociation radii of AGB stars in the cluster environment are similar to those of the intracluster UV field strength (Figures 5–7). The difference is that the former are determined by the intensity in SiO dissociation lines, while the latter characterize the continuum UV irradiation.

During the AGB phase, stars change their locations in the cluster, therefore they are irradiated by variable UV flux. From analysis of \( R_{\text{pd, SiO}} \) in different snapshots for the same AGB stars, we find that the corresponding variations of \( R_{\text{pd, SiO}} \) are typically less than a factor of two.

It is insightful to compare the derived photodissociation radii with the dust condensation zone in the CSE. The location of this zone is a matter of debate. According to theoretical models of dust condensation in outflows of M-stars, dust is formed at \( 5–10 \) photospheric stellar radii \( R_☉ \) (e.g., Gail & Sedlmayr 1999; Ferrarotti & Gail 2003). Nanni et al. (2013) recently derived smaller radii for dust condensation of \( 2–3R_☉ \) using models similar to that mentioned above with an alternative mechanism of dust destruction. A smaller condensation radius is also required by dynamical models of CSE of M-type AGB stars.
Observations of spatially resolved envelopes yield values varying from a few to $R_{10}^*$ (e.g., Zhao-Geisler et al. 2012; Khouri et al. 2014). We highlight the radii from 2 to $R_{10}^*$ in Figure 8 as the dust condensation zone.

As expected, $R_{pd,SiO}$ due to photodissociation by the interstellar UV photons lies outside the dust formation zone in all clusters even without dust shielding. The cluster UV photons penetrate much deeper in the CSE, reaching the dust condensation regions in a significant fraction of stars. A common feature for all model clusters is that the initial segregation of stellar mass has a strong impact on $R_{pd,SiO}$ owing to the higher stellar density of both irradiating and AGB stars in the central regions of clusters.

Figure 9 illustrates the dependence of the SiO photodissociation radii on the adopted dust-to-gas ratio $D$ in the shell. The figure shows $R_{pd,SiO}$ for stars in the $5 \times 10^4 M_\odot$ cluster and the dust-to-gas ratio $D = 0$, $10^{-3}$, and $10^{-4}$. Similarly to other models, the intracluster radiation field in this cluster has the largest impact on SiO in the shells of more massive AGB stars ending their life during the first 100 Myr. In the dust-free case, 54% (18%) of stars have $R_{pd,SiO} < 2 R_*$ in models with (without) IMS. For $D = 10^{-4}$, $R_{pd,SiO}$ is noticeably pushed outside due to dust shielding. There are no stars with SiO envelope within $2 R_*$.

The fraction increases to 60% (20%) for our upper limit for the condensation radius of $10 R_*$ in the models with (without) IMS. The ratio $D = 10^{-3}$ provides sufficient attenuation to block dissociating photons from the dust formation zone. The intracluster radiation in this case does not affect the condensation process, but it reduces the extent of SiO envelopes from a

(Höfner 2008).
When there are more than four AGB stars in a snapshot, we calculate the total number of bound AGB stars with $R_{\text{pd, SiO}} < R_{\text{cond}}$ for three values of the condensation radius $R_{\text{cond}} = 2, 5,$ and $10 R_*$ discussed above for each simulated cluster. These numbers are used to derive the total fractions of massive AGB stars affected by the intracluster UV field by integration over the entire cluster mass range with the cluster mass distribution function. Table 2 shows the resulting fractions relative to the total number of bound massive AGB stars. It is derived using the total number of bound stars $N_{\text{AGB}}^{\text{bound}}$ given by Equation (6) in the denominator of Equation (7) instead of $N_{\text{AGB}}$. For $N_{\text{AGB}}^{\text{b}}$, we take the number of bound stars satisfying the condition $R_{\text{pd, SiO}} < R_{\text{cond}}$. The fractions of stars are shown for models with and without IMS for the dust-to-gas ratio values $D = 0$ and $10^{-4}$. For the dust-free case, $R_{\text{pd, SiO}}$ in the majority of AGB stars in clusters with IMS is deeper than the inner border of the dust condensation zone. The fractions of AGB stars in clusters affected by the intracluster field are lower in models without IMS, but still significant, 60% and 75% with $R_{\text{pd, SiO}} < 5 R_*$ and $R_{\text{pd, SiO}} < 10 R_*$, respectively. The numbers in Table 2 imply that even if minor refractory dust species are formed closer to the star, resulting in a dust-to-gas ratio of $\lesssim 10^{-4}$, shielding provided by these species is not sufficient and the intracluster UV field nevertheless may affect dust condensation in a large fraction of stars.

As discussed in Section 3.1, results of our dynamical models of SC evolution combined with the adopted distribution of young SCs imply that about 30% of all massive AGB stars evolve in isolation. To illustrate the relative importance of a cluster environment for the entire population of massive AGB stars (bound and unbound), we show the numbers of AGB stars with $R_{\text{pd, SiO}} < R_{\text{cond}}$ relative to the number of all massive AGB stars in Table 3. According to our model calculations, in the absence of dust shielding, the intracluster UV photons are able to penetrate in the CSE deeper than $10 R_*$ in 52%–64% and deeper than $2 R_*$ in 28%–42% of all massive AGB stars. The lower and higher values correspond to the models without and with IMS.

### 3.4. Implications for the Stardust Input From AGB Stars

#### 3.4.1. Revision of the Model Predictions for Presolar Grains

In the following, we revise the model predictions for the relative contributions of massive AGB stars to both the presolar grain inventory carried out in our earlier work (Gail et al. 2009). Gail et al. (2009) put forward a model that relates theoretical studies of dust condensation during the entire AGB stage and a model for chemical evolution of dust and gas in the solar neighborhood to the contribution of AGB stellar populations as a function of their initial mass and metallicity. This model suggests that 40% and 60% of silicate grains in the stardust population at the instant of solar system formation originate from low- and high-mass AGB stars, respectively.

In the present study, we can evaluate the maximum possible effect of the cluster environment on the contribution from AGB stars by assuming that dust condensation is completely suppressed in massive AGB stars with $R_{\text{pd, SiO}} < R_{\text{cond}}$ and adopting the largest dust condensation radius $R_{\text{cond}} = 10 R_*$. We use the same dust yields as in our earlier works (e.g., Zhukovska et al. 2008; Gail et al. 2009; Zhukovska 2014) based on dust condensation models in O- and C-rich stellar winds of AGB stars. These yields are derived for single stars. There are observations that some binaries develop a common envelope that allows a dust condensation process. Evolution of interacting binaries is poorly understood. There are currently no yields available for dust condensed in the common envelopes for the solar metallicity. Very recently, Zhu et al. (2015) estimated the contribution of dust from binaries for the Large Magellanic Cloud and found that it is four times lower than the dust input from single stars using the dust yields from Zhukovska et al. (2008).

We multiply the dust masses ejected by massive AGB stars by the factor $1 - \eta$, where $\eta$ is the fraction of stars with photodissociation radii $R_{\text{pd, SiO}} < R_{\text{cond}}$ listed in Table 3. For $\eta = 0.64$ taken for the IMS models, the corresponding revised value for the relative contribution of massive AGB stars to the O-rich presolar grains of AGB origin equals to 0.4. We conclude that, although including the SC environment may reduce the relative contribution of massive AGB stars to the presolar grains, the lower limit for the mass fraction of 40% is too high to help mitigate non-detection of grains from these stars in meteorites.

#### 3.4.2. Dust Production Rates

AGB stars are the main stellar source of dust production in the Galaxy. The present-day rate of dust injection from AGB stars at the solar galactocentric radius is $1.2 \times 10^{-3} M_\odot$ pc$^{-2}$.
Gyr$^{-1}$, out of which $2.2 \times 10^{-4} M_\odot$ pc$^{-2}$ Gyr$^{-1}$ is attributed to the silicate stardust injection rate, according to the models published in Zhukovska et al. (2008). The contribution from massive AGB stars is $8 \times 10^{-5} M_\odot$ pc$^{-2}$ Gyr$^{-1}$ or 35% of the silicate dust input from AGB stars. Assuming that dust formation is completely suppressed in the cluster stars with $R_{p,SiO} < 10 R_*$ as described above and multiplying the dust yields for $m \geq 4 M_\odot$ by the reduction factor $1 - \eta$ of 0.46, we attain a lower limit for the current injection rate for AGB stars of $1.8 \times 10^{-4} M_\odot$ pc$^{-2}$ Gyr$^{-1}$ corrected for the fact that a substantial number of massive AGB stars remain bound in their parent SCs. Thus including the effect of a cluster environment in dust condensation models can reduce the total injection rates of silicate dust from AGB stars by at most 20%.

In any case, if the total silicate production rates from AGB stars are decreased owing to the effects mentioned above, it should not affect the amount or composition of the interstellar dust mixture, since the mass fraction of stardust from AGB stars in the Milky Way is only 2% and it is dominated by

Figure 8. Photodissociation radius of SiO relative to photospheric radius $R_*$ in dust-free shells of massive AGB stars in star clusters of $10^3$, $10^4$, and $10^5 M_\odot$ (from top to bottom). Red symbols show results of calculations with dissociation only by the ISRF component, and blue symbols by the ISRF and intracluster UV photons. Left and right panels present results for $N$-body models with and without IMS, respectively. The gray area marks the dust formation zone.
carbonaceous grains. The majority of the dust mass is formed by accretion in the ISM (e.g., Dwek 1998; Zhukovska et al. 2008; Draine 2009).

4. DEPENDENCE ON THE INITIAL CLUSTER MASS–RADIUS RELATION

In this section, we discuss how alternative relations between the initial mass and radius of model clusters based on the TRR and CRR models affect our main conclusions. All initial parameters for these models are the same as for the MRR set of models (Table 1) with the exception of the initial radii.

In all sets of models, the IMS allows the majority of massive AGB stars to remain bound in clusters with mass above \( M > 10^3 \) \( M_\odot \). Without IMS, the MRR models for clusters with \( M > 2 \times 10^4 \) \( M_\odot \) are more affected by the tidal field than other models because of their larger initial sizes, but the number of ejected stars remains fairly low in all cases. The

Figure 9. Photodissociation radius of SiO relative to photospheric radius \( R_\text{p} \) in massive AGB stars in a star cluster with mass of \( 5 \times 10^4 \) \( M_\odot \) and dust-to-gas ratios of \( 0, 10^{-4}, \) and \( 10^{-3} \) (top, middle, and bottom panels, respectively). The meaning of the symbols is the same as in Figure 8. Each second snapshot is shown to reduce crowding of the figure.
fraction of massive AGB stars evolving in clusters is 68% (67%) with (without) IMS for the TRR models, and 72% (75%) for the CRR models, respectively. These numbers are not very different from the value of 70% for the MRR models.

The TRR models have a shallower slope of the mass–radius relation compared to the MRR models, 1/3 and 1/2, respectively. Therefore, the TRR models are characterized by a lower intensity of intracluster UV radiation field in SCs with $M_3 < 2 \times 10^4 M_☉$, and a more intense radiation field in clusters of higher mass. The former decrease in the field strength is more important, because about 80% of progenitors of massive AGB stars originate from clusters with $M_3 < 2 \times 10^4 M_☉$. These results are quantified in Table 4, showing the fraction of massive AGB stars in which the UV field penetrates the dust formation zone normalized to the number of these stars bound in clusters and to their total (bound + unbound) number. The numbers of AGB stars with radii of SiO photodissociation within the adopted values of $R_{\text{cond}}$ for the TRR models are lower than the corresponding numbers for the MRR models (Tables 2 and 3), but the difference is at most 10%.

The initial difference in the strength of the intracluster UV field compared with the reference models is much stronger for the CRR case, although it is smoothed to some extent by the tidal disruption of low-mass clusters during the simulations. In contrast to low-mass clusters, the sizes of massive clusters increase by less than two times at most and preserve the initial difference, which is about five times between the CRR and MRR models for the $10^5 M_☉$ SC. The impact of these compact massive SCs on the total fraction of stars affected by the UV field is diminished by the cluster mass distribution function, proportional to $M_C^{-2}$ (Section 2.2). Nevertheless, the photodissociation radii of SiO are generally smaller in the CRR models, resulting in higher numbers of stars with $R_{\text{phot}, \text{SiO}} < R_{\text{cond}}$ (Table 5). In particular, the fraction of bound massive AGB stars with $R_{\text{phot}, \text{SiO}} < 5 R_*$ and $D = 10^{-4}$ is 60% (42%) with (without) IMS for the CRR models, which is more than two times higher than for the MRR models. The fraction of bound stars with SiO envelopes within $2 R_*$, our most conservative value of the condensation radius, is 17% (25%) higher in the CRR models with (without) IMS and $D = 0$ compared to the MRR.

This small dependence on the adopted initial mass–radius relation is attributed to the important role of the galactic tidal field in evolution of low- and intermediate-mass clusters. It implies that our conclusions do not strongly depend on the initial conditions.

5. DISCUSSION AND CONCLUDING REMARKS

We investigate what fraction of massive AGB stars evolves in their parent SCs and the impact of cluster UV radiation on their CSE. The field stars in our model originate (i) from low-mass clusters that dissolve at the stage of emergence from the natal molecular cloud or (ii) by ejection from their natal SCs. The latter process is modeled using $N$-body simulations of dynamical evolution of SCs in the local Galaxy. We find that 70% of massive AGB stars are members of their parent SCs. This value can be lower if the fraction of stellar mass formed in SCs is lower as suggested by some works (Piskunov et al. 2008a; Kruijssen 2012). Half of all bound massive AGB stars reside in clusters with initial mass exceeding $5 \times 10^3 M_☉$.

Intracluster UV radiation is $10^2$–$10^3$ times stronger than the ISRF for stars of $6–7 M_☉$ and gradually decreases to a few times ISRF strength for $4 M_☉$ stars in all considered SCs. The UV field strength shows 10 times larger scatter toward lower values in clusters without IMS owing to a more spatially extended stellar distribution. For this reason, the cluster UV photons on average penetrate deeper in the circumstellar shells of AGB stars in model clusters with IMS.

We find that in the initial stages of dust formation the cluster UV photons are able to dissociate the SiO molecules in the dust formation zone in a large fraction of massive AGB stars. This implies that the dust condensation process may be suppressed or delayed by the intracluster UV field, similarly to the effect of the UV field of chromospheric origin (Beck et al. 1992). The fraction of affected stars depends on the adopted initial mass–radius relation for model SCs and the location of the dust-forming zone. The models with initial segregation of stellar mass are characterized by stronger UV fields and therefore smaller SiO envelopes. For our reference models, 80% (60%) of AGB stars bound in SCs with (without) IMS have SiO photodissociation radii within five photospheric radii. This fraction constitutes 56% (41%) of (all bound and field) massive AGB stars. This value is even higher, 60% (56%), if we assume the constant initial radius of clusters supported by some observations (Larsen 2004). Infrared surveys for dust-enshrouded giants in young SCs in the Magellanic Clouds point to a lack of reddened IR objects (van Loon et al. 2005b). However, they do find massive oxygen-rich AGB stars with dust emission signatures in some clusters. Our results imply that the sizes of SiO envelopes of AGB stars in clusters with ages $\lesssim 200$ Myr are smaller than those of their counterparts in the field population as seen in Figure 9. This may be used as an indicator that an AGB star is a cluster member.

Our findings have major implications for dust input from AGB stars at the solar galactocentric radius. Adopting the upper limit for the extent of the condensation zone $R_{\text{cond}}$ of $10 R_*$ and assuming that dust formation is completely suppressed in stars with SiO photodissociation radius $R_{\text{phot}, \text{SiO}} < R_{\text{cond}}$, we find that the effect of a cluster environment on dust condensation in the
CSE can reduce the total injection rates of silicate dust from AGB stars from $2.2 \times 10^{-4} M_\odot$ pc$^{-2}$ Gyr$^{-1}$ to $1.8 \times 10^{-4} M_\odot$ pc$^{-2}$ Gyr$^{-1}$, or at most by 20%. This value depends on the adopted dust yields and on the number ratio between AGB stars of low and intermediate mass, which is determined by the star formation history. Applying the same assumptions to the model of low and intermediate mass, we derived the formation history. Applying the same assumptions to the model of low and intermediate mass, which is determined by the star adopted dust yields and on the number ratio between AGB stars from $\sim 3-4 M_\odot$ also experience hot-bottom burning (Busso et al. 1999; Marigo 2007; Ventura et al. 2012), they will be less affected by the intracluster UV field, since after 220 Myr its strength becomes comparable to or weaker than the ISRF. Consequently, the fractions of massive AGB stars affected by the intracluster field would decrease if we extend the considered mass range toward lower masses.

In our simple estimate, we did not consider dissociation of molecules that may be precursors of minor dust species with higher condensation temperature, e.g., corundum ($\text{Al}_2\text{O}_3$) and spinel ($\text{MgAl}_2\text{O}_4$) grains. We demonstrated that a low dust-to-gas ratio of $10^{-4}$ may mitigate the penetration of the UV photons in the base of the dust formation zone. Minor oxygen-bearing dust species with higher condensation temperature can thus assist formation of silicate grains by blocking the UV irradiation. Clumpiness in the shell is another factor currently neglected in our study that can provide local shielding from UV photons and enable dust formation.

Most mass is lost by evolved stars during the last few thermal pulsates of AGB evolution (superwind phase). A possible implication of the results derived in this work is that the superwind stage may be delayed in most massive AGB stars in clusters owing to suppression of initial condensation by UV irradiation of the CSE.

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**Table 4**

| $R_{\text{comb}}/R_{\odot}$ | Relative to the Number of these Stars Bound in SCs | No IMS | Relative to the Number of All Massive AGB Stars | IMS | No IMS |
|-----------------------------|-----------------------------------------------|--------|-----------------------------------------------|-----|--------|
| $D = 0$                     |                                               |        |                                               |     |        |
| 2                           | 0.53                                          | 0.02   | 0.31                                          | 0.03| 0.37   |
| 5                           | 0.74                                          | 0.21   | 0.51                                          | 0.09| 0.53   |
| 10                          | 0.89                                          | 0.57   | 0.70                                          | 0.34| 0.63   |

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**Table 5**

| $R_{\text{comb}}/R_{\odot}$ | Relative to the Number of these Stars Bound in SCs | No IMS | Relative to the Number of All Massive AGB Stars | IMS | No IMS |
|-----------------------------|-----------------------------------------------|--------|-----------------------------------------------|-----|--------|
| $D = 0$                     |                                               |        |                                               |     |        |
| 2                           | 0.77                                          | 0.05   | 0.66                                          | 0.02| 0.54   |
| 5                           | 0.86                                          | 0.60   | 0.78                                          | 0.42| 0.60   |
| 10                          | 0.92                                          | 0.79   | 0.88                                          | 0.69| 0.64   |
