A structural approach to 3D-printing arterial phantoms with physiologically comparable mechanical characteristics: Preliminary observations

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Abstract
Pulse wave behavior is important in cardiovascular pathophysiology and arterial phantoms are valuable for studying arterial function. The ability of phantoms to replicate complex arterial elasticity and anatomy is limited by available materials and techniques. The feasibility of improving phantom performance using functional structure designs producible with practical 3D printing technologies was investigated. A novel corrugated wall approach to separate phantom function from material properties was investigated with a series of designs printed from polyester-polyurethane using a low-cost open-source fused filament fabrication 3D printer. Nonpulsatile pressure-diameter data was collected, and a mock circulatory system was used to observe phantom pulse wave behavior and obtain pulse wave velocities. The measured range of nonpulsatile Peterson elastic strain modulus was 5.6–19 to 12.4–33.0 kPa over pressures of 5–35 mmHg for the most to least compliant designs respectively. Pulse wave velocities of 1.5–5 m s⁻¹ over mean pressures of 7–55 mmHg were observed, comparing favorably to reported in vivo pulmonary artery measurements of 1–4 m s⁻¹ across mammals. Phantoms stiffened with increasing pressure in a manner consistent with arteries, and phantom wall elasticity appeared to vary between designs. Using a functional structure approach, practical low-cost 3D-printed production of simple arterial phantoms with mechanical properties that closely match the pulmonary artery is possible. Further functional structure design development to expand the pressure range and physiologic utility of directly 3D-printed phantoms appears warranted.

Keywords
Arterial phantom, cardiovascular system mechanics, waveforms: hemodynamics, pulse wave, functional structure, physiologic elasticity, pulse wave velocity, 3D-printed phantom, additive manufacturing

Introduction
Waves drive blood through the arteries and there is a continuous energy exchange between pressure, flow, and arterial wall strain.¹⁻³ Hemodynamics,⁴,⁵ particularly wave mechanics,⁶,⁷ are important in cardiovascular pathophysiology,⁸ however the basis of the arterial pulse wave has not been elucidated.¹ While arterial phantoms have value in pulse wave mechanics research,⁹⁻¹¹ arterial architectural and nonlinear behavior complexities limit the utility of phantoms made from commercially available tubular elastomers.¹¹⁻¹⁴ Although complex phantom architectures are producible with 3D printed mold techniques,¹⁵ practical direct 3D-printing of robust, distensible phantoms with physiologically comparable properties suitable for studying wave mechanics is not reported.¹⁶⁻¹⁸ A major limitation is the cost and adaptability of the commercial 3D-printing elastomer technologies capable of printing complex geometries. Also, arteries stiffen with...
increased distension\textsuperscript{19,20} in contrast to the generally linear elastic response of elastomers.

In simplistic terms, the most important aspects of a phantom used to study wave mechanics are wall mechanical properties, which determine speed of the pulse through strain energy storage and luminal morphology which determines wave reflection. The interaction of these two characteristics along with the amplitude and frequency of the inlet (driving) fluid pulse determine the behavior of the pulse wave.\textsuperscript{1} Pulse wave velocity is generally conserved across mammals, with aortic values ranging from 4 to 13 m s\textsuperscript{-1} \textsuperscript{8,21–27} while pulmonary arterial velocities are reported in the range of 1–4 m s\textsuperscript{-1} \textsuperscript{28–35} To have relevance in terms of pulse wave mechanics, an ideal phantom would exhibit physiologic wave speeds and forms at physiologic pressures. Systemic mammalian mean arterial pressures (mean/peak) are 100–120/120–140 mmHg and 160–180/180–220 mmHg at rest and exercise respectively,\textsuperscript{36–40} while pulmonary arterial pressures (mean/peak) double from 15 to 20 mmHg at rest to 25–40 mmHg during exercise in most species.\textsuperscript{41–45}

To ultimately obtain physiologic wave speeds and reflective behavior, our phantom development philosophy is to first develop simple 3D printable tubular phantoms with wall properties that replicate arterial mechanical behavior and then develop techniques to produce phantoms with the more complex shapes associated with physiologic wave reflection phenomena. As a first step, we sought to separate phantom function from the generally linear elastic inherent properties of 3D printing polymers by developing structural wall designs intended to produce mechanical properties similar to those of arteries.

In prior work, tubes with circumferential wall spring elements that reduced stiffness and imparted nonlinear elasticity were designed and then produced with a low-cost fused filament fabrication 3D-printing technique.\textsuperscript{46} The objective of the current study was to determine if these tubes had properties suitable for the study of arterial wave mechanics. Pressure-diameter relationships were obtained, pulse wave velocity was measured over a range of pressures, and wave behavior was observed.

\textbf{Methods}

\textbf{Phantom designs}

Phantom circumferential elastic behavior was decoupled from the base material properties by using a spline function to generate the phantom circumference resulting in wall corrugations (Figure 1). Corrugation groove alignment with flow direction coupled with corrugation size to tube diameter ratios of $< 0.05$ suggests that corrugations would have little effect on fluid dynamic events associated with wave propagation.\textsuperscript{47,48} Previously, corrugated wall uniaxial behavior was found to be determined by corrugation size and pitch as well as wall thickness.\textsuperscript{46} To estimate the potential performance range of the structural-function approach, five corrugated designs differing by one or more of corrugation size, pitch or wall thickness were evaluated along with a smooth wall design for comparison to typical phantom constructs. One phantom of each design was produced from polyester-polyurethane (Elastollan\textsuperscript{®} BASF, Germany) based filament (TPU-60A Spool3D, Canada) using previously described techniques.\textsuperscript{46} Phantoms were printed to a height of 160 and 35 mm ID polyurethane end fittings were bonded, via polyurethane contact cement, reducing long axis free length to 150 mm (Figure 1). Due to thermal contraction inherent in fused filament printing and wall flexion during the printing process, printed corrugation size was smaller and wall thickness greater than the design parameters. As-printed phantom parameters are detailed in Table 1 and phantom cross-sectional scans of the corrugated phantoms are shown in Figure 2.

\textbf{Pressure-diameter}

Phantoms were horizontally mounted between the inlet and central bulkheads of a rail mount system. The central bulkhead was mobile, allowing adjustment of the phantom installed length. To avoid buckling\textsuperscript{49} during luminal pressurization, the free phantom length between end fitting inner faces was fixed at 160 mm resulting in $\sim 10$ mm pretension ($\lambda_{xz} \sim 1.07$) for all.
designs. To avoid sagging when filled, phantoms were immersed in an open water filled trough attached to the inlet and outlet bulkheads (Figure 3(a)). A large-bore water manometer in conjunction with sequential manual operation of ball valves located in tubing connected to the inlet and outlet bulkheads was used to pressurize the phantoms (Figure 3(b)–(d)) over a 40–60 s period to near steady state followed by a 10–20 s period of depressurization. During each pressure/depressurization cycle diameter was measured with a laser micrometer (LS9120 Keyence, Canada) positioned at the mid axial length (80 mm from the inner face of the inlet end fitting) for all phantoms. Additionally, to objectively demonstrate axial anisotropy and end constraint effects, design G was surveyed along its entire length in 5 mm increments. Pressure was measured via an electronic pressure catheter (FTS-5011B-0048D, Transonic-Scisense Inc. Canada) positioned at the phantom long axis and radial midlines. Signals were recorded at 100 sps with a data acquisition system (DT9826, Measurement Computing Corporation, USA).

Raw pressure and diameter data were filtered with a Savitzky-Golay filter and independently differentiated (after Parker) with respect to time by convoluting each signal with its first order Savitzky-Golay derived differentiation filter. Elastance (dP/dD) and compliance (dD/dP) differentials were obtained by both Savitzky-Golay convolution and direct sample-to-sample difference methods. An additional Savitzky-Golay filter was applied post differentiation to the Savitzky-Golay convolution method but not to the direct method differentials. Savitzky-Golay method differentiation and post differentiation filter parameters were recursively adjusted to minimize distortion of the smoothed Savitzky-Golay method results relative to the direct method (Supplemental Figure 1). Optimized results from the Savitzky-Golay method were used for

**Table 1. As-printed phantom parameters.**

| Design type | Nominal diameter (mm) | Circumferential corrugation count | Corrugation pitch (mm) | Corrugation size (mm) | Wall thickness (mm) |
|-------------|------------------------|----------------------------------|------------------------|-----------------------|---------------------|
|             |                        |                                  | Mean                   | SD                    | Mean                | SD                  |
| A 35        | None                   | -                                | -                      | -                     | 0.240               | 0.009               |
| D 35        | 48                     | 2.291                            | 1.523                  | 0.021                 | 0.276               | 0.014               |
| E 27        | 60                     | 1.412                            | 0.915                  | 0.010                 | 0.239               | 0.006               |
| F 27        | 72                     | 1.178                            | 0.935                  | 0.015                 | 0.248               | 0.009               |
| G 27        | 96                     | 0.884                            | 0.892                  | 0.014                 | 0.213               | 0.011               |
| H 27        | 96                     | 0.884                            | 1.513                  | 0.020                 | 0.227               | 0.008               |

Morphometric analysis of scanned images used to estimate corrugation size (10 measures) and wall thickness (20 measures). Corrugation pitch determined from nominal diameter and size is distance between inner and outer corrugation apices (see Figure 2). As designs E–H were anticipated to be more distensible, a smaller diameter was used to better match phantom lumen diameter at lower pressures to that of the pulsatile test system piping.

**Figure 2. As printed corrugated wall designs.** Images obtained by flatbed optical scanning of straightened unstrained phantom sections (~10 mm in length) cut in x-y plane at 30 mm build height, irregularities on and along section edges are associated with cutting artifacts. Letters denote design type, note variations in pitch between D through G and amplitude between D and H, complete metrics in Table 1. Scale bar applies to all sections. WT: wall thickness (mm); CP: corrugation pitch (mm); CS: corrugation size (mm).
Analysis. Analyzed pressure ranges and strain parameters are presented in Table 2.

**Table 2.** Diametrical strain parameters at phantom axial midpoint.

| Design type | Pressure range (mmHg) | Strain Maximum | Strain rate ($s^{-1} \times 10^{-2}$) |
|-------------|-----------------------|----------------|-------------------------------------|
|             | Start | End | Mean | SD | Mean | SD |
| A           | 5     | 90  | 0.21 | 0.015 | 5.57 | 0.137 |
| D           | 7     | 75  | 0.37 | 0.002 | 4.53 | 0.302 |
| D           | 10    | 50  | 0.24 | 0.011 | 5.77 | 0.148 |
| E           | 3     | 70  | 0.65 | 0.001 | 6.12 | 0.005 |
| E           | 5     | 45  | 0.45 | 0.001 | 7.68 | 0.197 |
| F           | 3     | 70  | 0.88 | 0.002 | 5.30 | 0.008 |
| F           | 5     | 45  | 0.61 | 0.002 | 6.53 | 0.020 |
| G           | 3     | 65  | 1.00 | 0.007 | 5.00 | 0.018 |
| G           | 5     | 45  | 0.66 | 0.005 | 5.55 | 0.008 |
| H           | 3     | 63  | 1.16 | 0.012 | 4.27 | 0.025 |
| H           | 5     | 45  | 0.91 | 0.004 | 4.47 | 0.001 |

Strain rate mean and standard deviation across analytical groups at 80 mm axial distance is $5.33 \pm 1.01 \times 10^{-2}$ respectively. Data recorded 80 mm from phantom inlet.

**Pulsatile behavior**

A water-based ex-vivo equine lung perfusion mock circulatory system, modified to house the rail mount system and improve pulse wave generation capability, was used to observe pulsatile behavior and determine pulse wave velocity (Figure 4). Briefly, a microcontroller-based pulse engine operated a pulse generation ball valve via a stepper motor (STM24QF-3AE Applied Motion Products Inc., USA) using closed loop servo positioning. A centrifugal pump drawing from a main reservoir generated system pressure. Pulse valve feed pressure was regulated by upstream bypass and inlet valves, which remained in fixed positions. Fluid and mechanical impulses were damped with a 360° flexible hose loop attached to a rubber and metal element between the bypass valve and inlet valves. Downstream of the pulse valve there was a magnetic flow meter (SM6000 ifm effector, Canada), a temperature indicator and a pressure transmitter for an over pressure protection system. The rail mount inlet bulkhead contained a check valve and there was a flat faced flow restriction element at the phantom outlet. A resistance valve, under open loop pulse engine control, was connected to the outlet bulkhead by flexible tubing. An anti-surge
reservoir with its spillover height set 50 mm above the phantom long axis midline was directly connected to the resistance valve.

Five Fr electronic pressure catheters (FTS-5011B-0048D, Transonic-Scisense Inc. Canada) were passed through 9 Fr introducer sheaths (CL-07900 Arrow International Inc, USA) contained within low clearance guide tubes built into the rail mount system inlet and central bulkheads. Relative motion between the catheters and introducer sheaths was eliminated by a locking plug inserted between them with catheter protrusion fixed at 30 mm to minimize motion and introducer sheath flow disturbance. The central bulkhead was positioned to create a 160 mm inter flange phantom length, generating 10 mm prestretch. The catheter sensing elements were positioned before phantom installation with a gage block mounted, mm graduated, rule after which the introducer sheaths were fixed in place via gland fittings at the bulkhead guide tube entrances. This arrangement precisely located the sensing elements relative to the phantom ends and each other and allowed accurate repositioning by advancing or retracting the introducer sheaths within the bulkhead guide tubes. During pulse wave velocity data collection, the proximal and distal pressure sensors were placed 30 mm from the inlet and outlet ends of the phantom respectively, resulting in 100 mm sensor separation. At this spacing the introducer sheath ends were flush with the rigid guide tube outlets minimizing catheter motion induced signal noise.

Pulse valve open position, time to reach open position, dwell time at open position, time to close, pulse frequency and static resistance valve position were controlled by the pulse engine. These parameters formed a pulse profile which, along with the bypass and inlet valve positions, anti-surge reservoir height and phantom mechanical properties determined pulse wave characteristics. Nine pulse profiles were developed (Table 3) to produce a range of five mean wave pressures (example Figure 5(a)) in each design and optimize wave foot transition clarity. Pulse wave velocity was calculated from wave foot minimum fiduciary points and by statistical phase offset applied to an analysis window selected to encompass a region of proximal and distal wave shape similarity in the runoff phase. Design G pulse profile 2 wave behavior was characterized with sequential data obtained by positioning the pressure sensors at the phantom long axis midpoint then retracting by 5 mm increments until sensors were 5 mm from each phantom end.

Figure 4. Schematic representation of mock circulatory system. A microcontroller-based pulse engine generates repeatable fluid pulses by controlling pulse valve open position, open and close rates and open dwell time as well as pulse period and resistance valve position. Anti-surge reservoir spill over height determines terminal runoff pressure. Phantom is horizontally mounted via rail mounted bulkheads and supported in water trough. Data acquisition system records proximal and distal intraluminal pressures, inlet flow rate and pulse valve position. Pump vibrations and water hammer impulses are damped by a looped hose fixed to a rubber and metal element. Protection system prevents phantom over-pressurization.

P: pressure; T: temperature; F: flow.
Electrical, fluid dynamic and mechanical noise were reduced by collecting data in 50 wave sets and analyzing the time synchronous ensemble average of the individual pressure waves (Supplemental Figure 4), inlet flows and pulse valve positions. All signals were sampled at 10 ksps and the data acquisition system (DT9826, Measurement Computing Corporation, USA) received a synchronizing signal from the pulse engine. Savitzky-Golay filtration was applied to individual and ensemble data. Pressure signals were preamplified (FP895B Transonic-Scisense Inc, Canada) and temperature drift was compensated by matching no flow pressures to anti-surge reservoir height. After initiating pulsatile flow, data collection commenced once the pulse wave form stabilized. Water temperature was recorded manually for each wave set. Design G relationships between pulse profiles and resultant pressure waves are shown in Figure 5(b) to (f).

**Results**

**Pressure-diameter**

Compliance on 5mmHg pressure isobars along the long axis of design G demonstrate longitudinal anisotropy, circumferential nonlinearity and end constraint effects (Figure 6). Design A (smooth wall) was considerably stiffer than the corrugated designs and its elastance response was near linear at lower pressures but declined at pressures > ~50 mmHg versus corrugated designs which stiffened with increasing pressure up to ~30–50 mmHg (Figure 7(a)). Over pressures of ~5–35 mmHg, the non-pulsatile Peterson elastic strain modulus of the corrugated designs increased with increased pressure, ranging from ~5.6–19.0 to ~12.4–35.1 kPa for the most to least compliant designs respectively and differences in Peterson elastic strain moduli between designs were consistent with respective differences in elastance response (Figure 7).

**Pulsatile behavior**

Minimum wave pressure (pressure at end of runoff phase), pulse pressure (difference between minimum and maximum wave pressures), pulse volume, maximum inlet flow rate and water temperature data over five pulse profiles for all designs are shown in Table 4.

Pulse pressure and volume relationships relative to minimum wave pressure appeared to vary between design types (Figure 8). Design A had smaller pulse pressures and pulse volumes relative to minimum pressures compared to corrugated designs and pulse pressure declined slightly with increasing minimum pressure versus the corrugated designs which demonstrated increased pulse pressure with increased minimum pressure. Corrugated design pulse volume response to increased pressure was blunted at the highest-pressure pulse profile. Pulse pressure normalized pulse volume response when normalized to corrugation size is correlated to phantom corrugation number ($R^2 = 0.79$, $p < 0.01$) and when normalized to corrugation number, likely proportional to corrugation size (Figure 8(b)).

Foot-of-wave pulse wave velocity, as determined by foot-of-wave fiduciary point (Figure 9(a)), in the corrugated designs increased with mean wave pressure (~1.5–5 m s$^{-1}$/~7–55 mmHg respectively) compared to the smooth wall design in which pulse wave velocity decreased with increasing mean wave pressure (~10–5.5 m s$^{-1}$/~10–75 mmHg respectively). Foot-of-wave pulse wave velocity analysis did not clearly identify differences between corrugated designs, however pulse wave velocity of the secondary wave in the runoff phase did appear to differ with designs (Figure 9(b)). Over mean analysis window pressures of ~5–65 mmHg corrugated phantom pulse wave velocities determined by statistical phase offset varied from ~1.4 to 3.1 m s$^{-1}$ respectively and there appeared to be a consistent inverse relationship between size and number of corrugations and pulse wave velocity across designs (Figure 9(b)).

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**Table 3. Pulse engine pulse profiles.**

| Pulse profile number | Pulse valve open time (ms) | Pulse valve dwell time (ms) | Pulse valve close time (ms) | Pulse period (ms) | Maximum pulse valve position (%) | Resistance valve position (%) |
|----------------------|---------------------------|-----------------------------|-----------------------------|------------------|---------------------------------|-------------------------------|
| 1$^a$                | 150                       | 20                          | 150                         | 1000             | 50                              | 30                            |
| 2$^b$                | 126                       | 25                          | 200                         | 2000             | 60                              | 14                            |
| 3$^b$                | 250                       | 50                          | 200                         | 2000             | 60                              | 14                            |
| 4$^b$                | 255                       | 63                          | 255                         | 2000             | 85                              | 12                            |
| 5$^b$                | 255                       | 63                          | 255                         | 2000             | 90                              | 10                            |
| 6$^c$                | 200                       | 50                          | 225                         | 1008             | 40                              | 9                             |
| 7$^c$                | 200                       | 50                          | 225                         | 1008             | 60                              | 9                             |
| 8$^c$                | 200                       | 50                          | 225                         | 1008             | 80                              | 9                             |
| 9$^c$                | 200                       | 50                          | 225                         | 1008             | 100                             | 9                             |

$^a$All designs.
$^b$Designs D through H.
$^c$Design A.
A combined temporal and spatial interpolation of design G, pulse profile 2 pressure wave demonstrates shape variation along the phantom long axis (Figure 10).

**Discussion**

Long axis compliance anisotropy (Figure 6) limits the functional length of fused filament fabrication
phantoms and occurs due to wall instability, which increases with build height, causing corrugation shape alteration during the printing process. The zone of diametrical reduction associated with the end fittings approaches 20% of phantom length at higher pressures (Figure 6). While the inlet transition zone is analogous to aortic and pulmonary artery–heart base junctures, the outlet zone is not representative of distal arterial branching and transitional compliance. Increasing functional length and developing a more physiologic outlet termination will potentially improve phantom utility, particularly regarding wave behavior.

Corrugated phantom Peterson elastic strain moduli (Figure 7(b)) ranged from 5.6 to 19 kPa to 12.4 to 33.0 kPa over pressures of 5–35 mmHg for the most to least compliant design types respectively. In vivo Peterson elastic strain modulus in calves was found to be ~41 kPa at a mean pressure of ~64 kPa, while inflation testing of mouse pulmonary artery over 5–40 mmHg found a Hudetz’s modulus of ~27 kPa. As pressure-diameter testing strain rates (Table 2) were considerably lower (mean ~5.5 s⁻¹ × 10⁻²) than estimated pulsatile strain rates (1–2 s⁻¹), reported pressure-diameter data should be considered non-pulsatile and more comparable to inflation testing, versus typical in vivo Peterson elastic strain modulus data. The effectively concurrent distension along the phantom long axis during pressure-diameter testing would be expected to yield a lower elastic modulus compared to a traveling pulse wave, as constraint imposed by the downstream, and to a lesser extent upstream, undilated adjacent wall would be absent during nonpulsatile conditions. Also,
| Design A | Design D |
|----------|----------|
| Pulse profile | Pulse profile |
| P<sub>Min</sub> (mmHg) | P<sub>Pulse</sub> (mmHg) | V (ml) | Q<sub>Max</sub> (l·min<sup>-1</sup>) | T (°C) | P<sub>Min</sub> (mmHg) | P<sub>Pulse</sub> (mmHg) | V (ml) | Q<sub>Max</sub> (l·min<sup>-1</sup>) | T (°C) |
| 1 | 1.1 | 9.90 | 39 | 11.4 | 30.9 | 1 | 3.0 | 11.1 | 40.2 | 11.7 | 28.9 |
| 6 | 20.2 | 7.46 | 52.6 | 10.5 | 31.5 | 2 | 9.7 | 23.3 | 69.9 | 12.1 | 29.1 |
| 7 | 38.4 | 6.90 | 64.7 | 10.8 | 31.5 | 3 | 13.3 | 30.8 | 85.8 | 12.1 | 29.3 |
| 8 | 52.1 | 5.68 | 69.9 | 10.7 | 31.5 | 4 | 22.6 | 35.1 | 87.9 | 11.8 | 29.3 |
| 9 | 61.4 | 5.24 | 74.0 | 10.7 | 31.6 | 5 | 41.3 | 31.8 | 85.8 | 11.4 | 29.4 |

| Design E | Design F |
|----------|----------|
| Pulse profile | Pulse profile |
| P<sub>Min</sub> (mmHg) | P<sub>Pulse</sub> (mmHg) | V (ml) | Q<sub>Max</sub> (l·min<sup>-1</sup>) | T (°C) | P<sub>Min</sub> (mmHg) | P<sub>Pulse</sub> (mmHg) | V (ml) | Q<sub>Max</sub> (l·min<sup>-1</sup>) | T (°C) |
| 1 | 2.6 | 12.6 | 41.5 | 12.4 | 25.8 | 1 | 3.1 | 11.3 | 46.9 | 14.3 | 32.2 |
| 2 | 10.2 | 22.9 | 69.5 | 12.1 | 26.3 | 2 | 14.4 | 19.3 | 82.8 | 14.9 | 32.1 |
| 3 | 14.1 | 32.3 | 86.1 | 12.1 | 26.7 | 3 | 20.0 | 28.2 | 103.3 | 15.0 | 32.0 |
| 4 | 22.9 | 40.8 | 88.0 | 11.9 | 27.7 | 4 | 23.6 | 31.1 | 107.3 | 14.9 | 32.0 |
| 5 | 41.5 | 41.6 | 85.6 | 11.4 | 27.3 | 5 | 31.0 | 32.1 | 107.3 | 14.6 | 31.9 |

| Design G | Design H |
|----------|----------|
| Pulse profile | Pulse profile |
| P<sub>Min</sub> (mmHg) | P<sub>Pulse</sub> (mmHg) | V (ml) | Q<sub>Max</sub> (l·min<sup>-1</sup>) | T (°C) | P<sub>Min</sub> (mmHg) | P<sub>Pulse</sub> (mmHg) | V (ml) | Q<sub>Max</sub> (l·min<sup>-1</sup>) | T (°C) |
| 1 | 2.2 | 12.0 | 39.1 | 11.5 | 35.9 | 1 | 3.4 | 9.2 | 45.1 | 13.8 | 27.8 |
| 2 | 7.3 | 14.4 | 68.3 | 11.8 | 35.3 | 2 | 15.0 | 10.5 | 80.0 | 14.3 | 27.9 |
| 3 | 10.8 | 16.9 | 84.5 | 11.9 | 35.0 | 3 | 21.7 | 14.5 | 100.0 | 14.5 | 28.2 |
| 4 | 19.0 | 19.8 | 91.1 | 12.3 | 34.5 | 4 | 36.3 | 17.9 | 105.9 | 14.7 | 28.5 |
| 5 | 30.4 | 22.3 | 90.1 | 12.0 | 34.2 | 5 | 49.8 | 14.9 | 105.5 | 14.4 | 28.8 |

P<sub>Min</sub>: minimum pressure; P<sub>Pulse</sub>: pulse pressure; V: pulse volume; Q<sub>Max</sub>: maximum pulse flow rate; T: fluid inlet temperature during data collection.
the markedly lower strain rates compared to pulsatile conditions would be expected to result in decreased slope of the elastic response due to reduced viscoelastic effects. Consequently, the pressure-diameter method used should overestimate phantom compliance.

Elastance of the corrugated phantoms was nonlinear and markedly lower than the smooth walled design (Figure 7(a)). However, at higher pressures, likely due to a purely elastomeric material response as the corrugated spring elements become fully extended, corrugated design elastance becomes linear. This transition identifies the upper pressure limit of the physiologic response range for each design. The compromise between higher compliance and physiologic response range is evident from the corrugated phantom Peterson elastic strain moduli (Figure 7(b)); the modulus of design H is half that of design E but the slope declines at \( \sim 23\, \text{mmHg} \) pressure versus design E which maintains a physiologic profile to \( 35\, \text{mmHg} \). Both elastance and Peterson elastic strain modulus of the corrugated designs appear to have an inverse relationship to corrugation number or corrugation size.

Maximum inlet convective velocities (derived from volumetric flow rate, Table 4) ranged from \( \sim 0.17 \)–\( 0.23\, \text{m s}^{-1} \) across all designs and pulse profiles, suggesting that convective flow was not a significant contributor to pulse wave velocity. Variations in maximum flow rates were consistent with volume differences between pulse profiles within design types (Table 4) but lack of concurrent diameter data precludes analysis of reservoir function within and between designs. Corrugated phantom pulse volumes and pulse pressures appeared to vary between designs and were larger than the smooth wall design (Table 4, Figure 8(a)). Pulse volumes were largest in designs F and H and were similar across pulse profiles, but the less compliant design F generated nearly twice the pulse pressures as design H while pulse pressures in designs D and E were highest, pulse volumes were similar between them (Table 4, Figure 8(a)). The pulse volume was unchanged in design F and decreased in all other corrugated designs for pulse profile 5 versus 4 despite increased maximum pressure (Table 4). Increased outlet resistance via the resistance valve or increased elastance associated with higher pressure (Figure 7(a)) or both may have caused this effect. The inter phantom volume and pressure variations observed suggest design-based differences in reservoir behavior and pulse volume normalized to pulse pressure and corrugation size was found to be correlated to number of corrugations (Figure 8(b)).

Design A pulse wave velocity was fastest (\( \sim 10\, \text{m s}^{-1} \) at a mean wave pressure of \( \sim 10\, \text{mmHg} \)), as predicted by its elastance (Figure 7(a)) and declined to \( \sim 5\, \text{m s}^{-1} \) when the mean wave pressure was \( \sim 77\, \text{mmHg} \) (Figure 9). This non-physiologic response is expected for a smooth wall phantom as the base material elasticity decreases with stretch (Figure 7(a)) while the wall...
(hoop) stress increases directly with diameter and inversely with thickness. The non-physiological pulse wave response of smooth wall phantoms is also predicted by the Moens-Korteweg equation which defines a proportional relationship between pulse wave velocity and the square root resulting from the product of the incremental elastic modulus and wall thickness divided by the tube radius. Conversely, corrugated phantom pulse wave velocities increased with increasing pressure (Figure 9) in a physiologically consistent manner within their respective nonlinear response ranges (Figure 7). Pulse wave velocities obtained were 1.4–5 m s\(^{-1}\) over mean wave pressures ranging from 7 to 45 mmHg respectively for speed at the foot of the wave and of 1.4 to 3.4 m s\(^{-1}\) over runoff analysis window mean pressures of 4–45 mmHg respectively (Figure 9).

Interestingly, runoff wave velocity appeared to better differentiate corrugated design type versus foot-of-wave velocity (Figure 9), and the differentiation matches the relative speed differences anticipated from the design parameters (decreased stiffness with increased corrugation number and/or corrugation size) and predicted by the pressure-diameter testing (Figure 6). The differences in pulse wave velocity differentiation of design types between the analysis methods may be a consequence of reduced fluid dynamic environment complexity during runoff, where flow wave effects and rapid changes of wall stiffness are minimized. While regions of waveform similarity between distal and proximal waves in the runoff phase were found for most phantom and pulse profile combinations, differences were observable which may have affected accuracy of the statistical phase offset technique. Pulse wave velocity variation throughout the evolution of the pulse wave in time and distance also needs to be considered.

Secondary wave (Figure 5) characteristics are illuminated by the temporal-spatial pressure wave representation (Figure 10). The near uniform periodicity and remarkable attenuation of the superimposed wave at phantom mid length suggests that it may be a trapped reflected wave. Wave trapping is expected given the relatively short phantom length and powerful reflective sites arising from the abruptly reduced diameter and increased stiffness (Figure 6) associated with the phantom end fittings. Considering the temporal-spatial totality of the pressure wave (Figure 10) in conjunction with inlet fluid pulse timing (Figure 5) suggests a basis for the shape of the pressure wave. The main wave results from the pressure rise generated by inlet fluid pulse momentum working against the outflow resistance. The springs formed by the phantom wall corrugations are stretched by the pressure and moderate the pressure rise rate and magnitude by storing fluid volume and strain energy. As inlet flow ceases, spring strain energy is released, driving out the stored volume, resulting in gradual pressure attenuation. A second presumably persistent reflected wave appears early in the inflow phase and is superimposed on the main wave. Based on the observed pressure-flow behavior, it seems likely that exposing a series of phantoms with different

**Figure 9.** Relationship between phantom pulse wave velocity and mean wave pressure for pulse wave velocities obtained from foot-of-wave (FOV) fiduciary point analysis (a) and from statistical phase offset analysis of waves present in the runoff phase (b). Letters denote design types. In contrast to the smooth wall phantom (A), pulse wave velocity determined by foot-of-wave analysis for the corrugated phantoms (D–H) increases with increasing pressure. Corrugated phantom pulse wave velocities determined by foot-of-wave analysis are similar for all designs whereas wave velocities during runoff appear to have an inverse relationship to corrugation number or size.
Figure 10. Interpolation of repeated pressure waves surveyed along phantom long axis in 5 mm increments from inlet. First 1250 of 2000 ms pulse duration shown. Note attenuation of secondary wave at phantom midpoint (80 mm distance). Design G, pulse profile 2.

mechanical and reflective properties to a range of precisely repeatable inlet fluid pulses while measuring pressure, flow, and diameter along the length of the phantoms would support further development of wave intensity and reservoir function analysis. This approach may provide new insights into the mechanistic basis of the pulse wave.

Multiple copies of each design type were not produced, and repeated measures were not obtained for pulsatile data, consequently results cannot be stated with statistical confidence. However, based on the relatively simple and automated nature of the 3D printing process and the reproducibility observed during the development process, it is reasonable to expect repeatability of corrugation form and function within design types in future trials. In this study, the corrugated designs were consistently differentiated by corrugation number and size for all analysis except foot-of-wave pulse velocity where pulse wave velocity values were similar. The study did not allow for minor differences in wall thickness to be evaluated. Increasing axial pretension has been reported to lower circumferential stiffness in elastomeric tubes and this effect would be expected to lower pulse wave velocity. Conversely, effective circumferential stiffening away from the phantom midsection due to end fixation would increase the regional pulse wave velocity. While this aspect of phantom behavior was not examined, as pretension was consistent between designs and effects likely modest, pretension is unlikely to interfere with comparison of compliance and pulse wave velocity between designs or to previously reported pulse wave velocities obtained in 3D printed phantoms. Temperature effects were not investigated; during pulsatile data collection fluid temperature varied up to 1.7°C within designs and 8.1°C between designs (Table 4). Wall stiffness and pulse wave velocity would be expected vary inversely with temperature. However, the lowest pulse wave velocities were observed for design H (Figure 9(b)), which was tested at the lower end of the temperature range, suggesting that design features rather than temperature caused the pulsatile behavior differences observed between phantoms.

Unlike water, blood is a non-Newtonian fluid with a slightly higher density and its viscosity varies with flow, temperature, and geometry. Consequently, more sophisticated phantom based hemodynamic studies will benefit from the use of blood mimicking fluids such as glycerol solutions. Elastomers based on polyurethane and silicon are generally compatible with a broad range of chemicals and are commonly utilized in low modulus additive manufacturing techniques. The polyester-polyurethane compound used to produce the phantoms in this study is particularly resistant to fats and oils including glycerol, which combined with its excellent printing and bonding characteristics, make it well suited for development of structurally functional hemodynamic phantoms.

This study simply demonstrates the short-term potential to create more elaborate corrugated wall phantoms that may be useful for studying wave mechanics in distensible tubes. The immediate application of the structure function approach to other arterial phantom applications such as flow visualization is not obvious. However, by separating material properties from phantom wall elasticity, this approach expands the range of materials that can be used to create distensible phantoms, potentially including those with light characteristics suitable for visualization studies.

The observations from this study are compelling enough to encourage further development of the functional structure approach to 3D printed arterial phantoms. Of particular importance is expanding the nonlinear behavior pressure range beyond the 23–45 mmHg achieved in this study to encompass the broad range of normal and pathophysiologic conditions in both the pulmonic and systemic circulation of humans and animal models. Resolving long axis anisotropy, replicating axial-circumferential strain relationships and practical production of complex geometry including, tapering, positive and negative reflection sites, branching, and curvature are also essential developments. Avenues to pursue these objectives include corrugation design optimization using advanced design tools that integrate complex architectures with mathematical surface definitions, and implementation of light-based elastomer 3D printing processes which will allow production of more intricate corrugate features with better design fidelity than is currently achievable with fused filament fabrication techniques.

Conclusions

To the extent of the authors’ knowledge, this work demonstrates the first successful direct 3D-printed production of a range of robust arterial phantoms with pulse wave velocities on the order of 1.5–5 m s\(^{-1}\), less than half of previously reported wave speeds.17
within the range of pulmonary artery pulse wave velocities reported in humans and other species. This result was achieved via corrugated wall designs that separated phantom function from the mechanical properties of the polyurethane polymer construction material by creating nonlinear circumferential springs in the phantom walls. Importantly, the phantoms demonstrated design driven nonlinear elastic behavior with walls that stiffened with increased pressure, matching the physiologic response of arteries. Continued development of phantom production techniques, mock circulatory systems and instrumentation may produce novel knowledge regarding arterial pulse wave mechanics.

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