1. Introduction

One of the key-science goals of the SKA is to detect most of the neutral hydrogen (HI; 1420.4 MHz in the rest frame) content of galaxies out to cosmological redshifts of $z \sim 1$ (for further details see e.g. Science with the Square Kilometre Array eds. Carilli and Rawlings or Cosmology, Galaxy Formation and Astroparticle Physics on the Pathway to the SKA eds. Klöckner, Rawlings, Jarvis and Taylor). The technical parameters that determine the performance of the SKA have been identified previously during the SKADS program and are defined in the Benchmark scenario (Alexander et al. 2007). At the moment the SKA design includes three distinct telescope technologies in order to cover the required frequency range, i.e. between a few hundreds of MHz to 10–25 GHz. The parameter space one needs to cover to assess the performance of the low-frequency sparse dipole array, the mid-frequency aperature array (AA), or the high-frequency dish array is enormous, and this is impossible to accomplish via a single telescope simulation. To get a basic understanding of the array parameters and their influence on the quality and sensitivity of the final images, one can parameterise each of the different antenna types in terms of a dish equivalent. For a dish array, two basic parameters are the system equivalent flux density (SEFD) and the image sensitivity ($\Delta I$). Respectively, these are given by

\[ \text{SEFD} = \frac{T_{\text{sys}} 2k}{\eta_a A}, \]  

\[ \Delta I = \frac{\text{SEFD}}{\sqrt{N(N-1)N_{\text{Stokes}} t \Delta \nu}}, \]  

where $T_{\text{sys}}$ is the system temperature [K], $k$ is the Boltzmann constant, $A$ is the collecting area [$m^2$], and $\eta_a$ is the aperture efficiency, and (for a naturally weighted image) the image sensitivity can be calculated via:

\[ \Delta I = \frac{\text{SEFD}}{\sqrt{N(N-1)N_{\text{Stokes}} t \Delta \nu}}, \]  

where $N$ is the number of Antennas, $N_{\text{Stokes}}$ is the number of Stokes parameters, $t$ integration time [s], and $\Delta \nu$ is the bandwidth [Hz] (Wrobel and Walker 1999). A sensitivity calculator can be found at wwwastro.physics.ox.ac.uk/~hrk/ARRAY..EXPOSURE.html).

In order to increase the image sensitivity both equations dictate that the system temperature and the effective area are crucial to the telescope performance. However in the case of continuum emission that is spectrally well-behaved (spectral index of around zero), the image sensitivity can be increased by trading the SEFD for increased bandwidth. For spectral line observations, where the bandwidth is tailored to the width of the expected signal, this cannot be done. Bandpass stability also plays a crucial role in the image quality in this regime.

In this article we describe an end-to-end (e2e) HI simulation plan that is focused on exploring a more manageable parameter space defined by the system temperature, effective area, and the spatial configuration of the array.

2. Simulation

Any aperture synthesis telescope acts as a spatial frequency filter and an analytic determination of the final image quality is in most cases impossible. Therefore the purpose of any interferometry simulation is to define a practical sensitivity limit with respect to the theoretical estimates. Generally one would like to have a full array simulation that simulates the complete signal path from the astronomical source up to and including the receiver electronics. Such an approach is very complicated, computationally expensive and for the purposes of a full SKA simulation completely impractical. The e2e simulation can be broken down into individual components each of which is treated as a standalone simulation. If one is interested in the electromagnetic properties (e.g. the directional gain and its stability) of individual dish designs one needs to take into account the telescope structure and make use of a full electromagnetic simulation (e.g. Holler et al. 2008). Similar simulations are needed if one is interested in the performance of an aper-
Fig. 1. Overview of a full simulation path.

A suite of Python-based routines with user-friendly GUIs, collectively known as the S3-Tools allows access, manipulation and imaging of the SKADS Simulated Skies. These tools have been developed by F. Levrier and a general overview can be found in this volume (Levrier, 2009 in these proceedings).

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2.1. The sky simulation

Here we present a short summary of the sky simulations that can be used within the array simulator. Further details on the simulations together with a webform which can be used to query the databases is available on the Oxford S3 webpage [s-cubed.physics.ox.ac.uk](http://s-cubed.physics.ox.ac.uk). The full suite of simulations is presented using two distinct products. Properties of individual extragalactic objects and of Galactic pulsars are stored in databases (SEX, SAX, PUL), whereas morphologically complex structures such as the Global Sky Model (GSM) and the signals of the Epoch of Reionization (EOR) are available as images.

The GSM is the radio foreground of our Galaxy which has been modeled by the radio and (sub)-millimeter emission between 10 MHz to 100 GHz. In addition to the diffuse Galactic emission it also includes emission from individual point sources e.g. supernova remnants [de Oliveira-Costa et al. 2008](http://space.mit.edu/home/angelica/gsm).

The EOR images display the HI line signal of the Intergalactic medium (IGM) during the Epoch of Reionization. This simulation covers the redshift range between \( z = 5.6 \) and \( z = 23.6 \). In addition to the ionization field, the effect of inhomogeneous heating of the IGM by X-rays and the Lyman-\( \alpha \) radiation field are taken into account. The simulations have been produced in a cubic simulation box with a side length of \( s_{\text{box}} = 100 \) Mpc/h and a particle mass resolution of \( 3 \times 10^6 \) solar masses (Santos et al. 2008).

The semi-empirical simulation of extragalactic sources (SEX) describes the radio continuum emission in a sky area of \( 20 \times 20 \) deg\(^2\) out to a cosmological redshift of \( z = 20 \). As the name suggests, the sources were drawn from observed (or extrapolated) luminosity functions and grafted onto an underlying dark matter density field with biases which reflect their measured large-scale clustering. This approach puts an emphasis on modelling the large-scale cosmological distribution of radio sources rather than the internal structure of individual galaxies.
Five source types of radio sources have been included in the simulation:

- Radio-quiet AGN [1 core; 36,132,566 sources]
- Radio-loud AGN of the FRI class [1 core + 2 lobes; 23,853,132 sources]
- Radio-loud AGN of the FRII class [1 core + 2 lobes + 2 hot-spots; 2,345 sources]
- Quiescent star-forming galaxies [1 disk; 207,814,522 sources]
- Starbursting galaxies [1 disk; 7,267,382 sources]

For each of the source types, the database provides the radio fluxes at observer frequencies at 151 MHz, 610 MHz, 1.4 GHz, 4.86 GHz and 18 GHz, down to flux density limits of 10 nJy. Intermediate frequencies can be determined by using the S3-tools. In addition to the continuum emission this simulation provides a rough estimate of the HI mass of the starbursting and star-forming galaxies (Willman et al. 2008). A second version of these simulations extending the simulated properties into the far-infrared (principally for comparison with observations which significantly affect the dynamic range and image formation) has now been completed (Willman et al. 2010).

The semi-analytic simulation (SAX) provides the properties of neutral atomic (HI) and molecular (H₂) hydrogen in galaxies and associated radio and sub-millimeter emission lines, i.e. the HI-line and various CO transition lines. This simulation relies on the Millennium simulation of cosmic structure (Springel et al. 2005), which reliably recovers comoving length scales from 10 kpc to several hundred Mpc and galaxies with cold hydrogen masses (HI+H₂) above $10^8 M_\odot$.

There are two versions of the SAX database, reflecting the different versions of the Millennium simulation: the full Millennium simulation ($s_{box} = 500/h$ Mpc; $\sim 685$ Mpc) and the smaller test version, called the Milli-Millennium simulation ($s_{box} = 62.5/h$ Mpc; $\sim 85.6$ Mpc) where $s_{box}$ defines the diameter of the simulated box. Both of the SAX databases have been produced by constructing a mock observing cone from the corresponding simulation box. The opening angle or the field of view (FoV) of these simulations therefore depends on the values of the maximum redshift one requires ($z_{max}$), e.g. for a redshift of 1 the FoV of the simulation would be $12\times12$ deg$^2$. More information about the FoV of the simulation can be obtained via the simulation page. Currently, radio continuum data is not available, although efforts are being made to add this information (Obreschkow et al. 2009a; Obreschkow et al. 2009b; Obreschkow et al. 2009c).

S3-Tools is used to build mock radio maps or cubes in which the radio emission of the extragalactic radio sources could be combined with the diffuse radio emission of the GSM or EOR.

### 2.2. Array simulation

The developed array simulator\(^3\) is based on “classical” AIPS and ParselTongue (Greisen 1990, Kettenis et al. 2006), the Python interface to AIPS. The core function of the array simulator makes use of the AIPS task UVCON. The basic input of this task is a list of antenna locations, together with properties of each antenna, such as diameter, system temperatures and aperture efficiencies. Additional inputs are the total time of observation, the integration time per visibility and the input sky model which also defines the pointing position on the sky. The output is a standard UV-FITS data file in which the visibilities correspond to the input model with added Gaussian noise appropriate for the specified antenna characteristics. Dirty or deconvolved images can be produced by invoking the task IMAGR. If the input model consists of a cube instead of a 2-D image then two different simulation paths can be used to generate the “observed sky”. If the output map is to be a continuum image formed at the central observing frequency, the visibilities are produced per frequency step and are finally merged into a single visibility set. If instead the output should be a 3-D datacube, the simulation produces a unique visibility set at each frequency step, each of which is then imaged independently. Each plane is finally combined into a cube by using the task MCUBE. For cases where the duration of the observation equals or exceeds that necessary for a full UV coverage, the visibilities are generated for a full synthesis and the noise scaled down accordingly. This cuts down on both processing overheads and the size of the resulting UV data files.

This style of simulation is well suited to the investigation of the completeness of surveys as well as to the understanding of the imaging capabilities when observing individual galaxies. In particular one can investigate the quality of snapshot observations for different array layouts. There are, however, several AIPS-based limitations which have a direct influence on the questions we can ask, and more complicated simulations are needed to address these. Currently the number of array elements which AIPS can handle is limited to 255 (E. Greisen 2009, private communication), which is sufficient for most of the current arrays but is not enough for a full simulation of, for example, the LOFAR array at the level of individual dipole elements. One can circumvent this to some extent by combining several elements into a single station. This is relevant since LOFAR does indeed perform correlations between the beamformed data from each station, and not between individual dipoles. This is a model which the SKA is likely to follow in order to minimize the data stream.

Two properties of a real interferometric array which are absent from this simulation framework are primary beam effects and bandpass variability. These are two factors which significantly affect the dynamic range and im-

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\(^3\) A copy of this simulator can be downloaded via www.astro.physics.ox.ac.uk/~hrk
age quality of a real observation, particularly the former in the case of an aperture array. Despite the various limitations we feel that AIPS is likely to be the most tested software package and our approach provides a basic simulation pipeline which can provide a reliable check for more complicated simulation efforts (e.g. within MeqTrees or CASA).

In the redshift range around $z = 1$ the SKA's mapping speed has the potential to be revolutionized by mid-frequency aperture arrays (AA). As mentioned before, the simulation software is limited to 255 antennas and it is necessary to combine the aperture arrays into individual stations. The following equation shows how to calculate the total area of an aperture array, assuming Hertzian dipoles, and therefore the equivalent dish diameter of an AA station:

$$A_{AA} = N_{tile} N_{dipole} \frac{3}{8} \pi \left( \frac{c}{\nu} \right)^2 N_{stokes},$$  \hspace{1cm} (3)

where $N_{tile}$ is the number of tiles and $N_{dipole}$ is the number of dipoles per tile. Assuming a square kilometre of collecting area the diameter of a SKA AA station would be 56 m. Note that an aperture efficiency of 80% and a total of 255 stations has been assumed for a $S^3$ default SKA realization ($S^3_{\text{real}}$). This value only corresponds to observations towards the zenith, and the effective station area varies with elevation. However simulations to investigate the performance of such a simplified AA are still valuable because the layout of the array will directly affect the synthesized beam and therefore the imaging capability. Figure 3 shows a cut through the dirty beam pattern showing a high sidelobe pattern which can be minimized by varying the station distribution within the array configuration (e.g. AntConfig can be used for this purpose; www.kat.ac.za/public/wiki/AntConfig).

The current design of the aperture array has two layouts that have the same core, but differ in the outer regions (R. Bolton 2009, private communication). The core has a radius of 2.5 km and has 165 randomly placed stations which are separated at least by 96 m.

- The “concentrated” layout has 72 stations beyond the core placed in 5 spiral arms out to 10 km (radius). Beyond this 13 stations are placed on the same spiral arms out to 180 km ($S^3_{\text{real}}C$).
- The “not-concentrated” layout has 85 stations beyond the core logarithmically placed in 5 spiral arms out to 180 km ($S^3_{\text{real}}NC$).

Figure 2 shows the UV coverage of a test simulation of 1 hour duration. For displaying purposes each visibility has an integration time of 10 minutes. The high density of visibilities and the filled central core will provide high sensitivity and image fidelity when observing diffuse HI emission. However deconvolution of such structure will be difficult because of the dirty beam pattern shown in Fig. 3. The broad sidelobe pattern will add ambiguities during attempts to recover diffuse, extended HI emission.

A final limitation of the simulation pipeline arises at the imaging stage. The images that can be handled by AIPS are limited to 8096 pixels per dimension. For the current SKA layout the maximum baseline length of 360 km would provide sub-arcsec angular resolution at frequencies higher than 200 MHz. Such resolution limits the field-of-view that can be simulated, and producing a simulation covering several square degrees requires the sky to be divided into sub-patches. For example, the spatial resolution...
AIPS limitation into account, such images would cover a pixel resolution of about 0.1 arcsec per pixel. Taking the Nyquist-sample the sky then these images need to have a reduced via Eq. 2.

The basic relationship between HI mass and HI line flux provides a general understanding of the detectability of HI. The following equation is given to provide a general understanding of the detectability of HI. The fractional HI mass range of the HIPASS survey. Note for detection arguments one needs to assume a channel resolution similar to the HI line width, otherwise the sensitivity is reduced via Eq. 2.

\[
M_{HI} = \frac{2.36 \times 10^5}{(z + 1)} D_L^2 \frac{\pi}{\sqrt{2ln(2)}} S_p \Delta V, \tag{4}
\]

where \(D_L\) is the luminosity distance [Mpc], assuming a Gaussian line profile where \(S_p\) is the peak flux density [Jy] and \(\Delta V\) is the full line width measured at half-maximum [FWHM; kms\(^{-1}\)]. To investigate how much of the HIPASS volume at redshift 1 a 4x4 deg\(^2\) field must be simulated and need to be split into 36 individual sub-array-simulations to handle the AIPS image limitation.

**Fig. 4.** Flux density of HI masses with a fixed line width of 164 kms\(^{-1}\) versus redshift. The three lines show the entire HI mass range of the HIPASS survey. Note for detection arguments one needs to assume a channel resolution similar to the HI line width, otherwise the sensitivity is reduced via Eq. 2.

**Table 1.** Simulation parameters at various redshifts. Bandwidth corresponding to a fixed redshift interval of \(\Delta z = 0.1\). The fraction of the HIPASS volume to the co-moving volume of 1 square degree and \(\Delta z = 0.1\) (e.g. at redshift 1 such volume would correspond to 0.0008 Gpc\(^3\) deg\(^{-2}\)). The FoV of the SAX sky simulations (values are obtained from s-cubed.physics.ox.ac.uk). Expected HI sources per square degree for a flux limit of 3 \(\mu\)Jy (assuming a rms of 1 \(\mu\)Jy). For example to investigate the HIPASS volume at redshift 1 a 4x4 deg\(^2\) field must be simulated and need to be split into 36 individual sub-array-simulations to handle the AIPS image limitation.

| redshift | bandwidth [MHz] | HIPASSvol co-volume [deg\(^2\)] | SAXsky | SAXsources |
|----------|-----------------|-------------------------------|--------|------------|
| 0.5      | 59              | 37                            | 21.4 x 21.4 | 15136      |
| 1        | 34              | 16                            | 12.0 x 12.0 | 7136       |
| 1.5      | 22              | 12                            | 9 x 9   | 1897       |
| 2        | 15              | 11                            | 7.5 x 7.5 | 816        |

of the array configuration at 700 MHz is 0.3 arcsec. If we Nyquist-sample the sky then these images need to have a pixel resolution of about 0.1 arcsec per pixel. Taking the AIPS limitation into account, such images would cover a sky area of 0.67x0.67 deg\(^2\) and thus to simulate a 4 deg\(^2\) field 9 sub-images are necessary.

### 2.3. The HI e2e simulation

The anticipated HI simulation will make use of the SAX simulated sky. These simulations do not include a physical model of the associated continuum emission. However, to evaluate the influence of continuum emission to the HI simulation a mock continuum component may be added to the line emission (using the task UVMOD). The HI emission of each galaxy has been pasted into the model cube by using S3-tools, selecting the “Oxford” HI templates in the map making tool. The following equation is given to provide a general understanding of the detectability of HI. The basic relationship between HI mass and HI line flux density is defined by

The FoV of the Millenium simulation box corresponds to an area of 116x116 deg\(^2\) at redshift 0.1, which shrinks to 5.4x5.4 deg\(^2\) at redshift 4. At low redshifts a HI simulation would help to investigate potential systematic errors in a measurement of the faint end of the HI mass function. Such a simulation would require around 30276 individual simulation runs, based on the field-of-view limitations per-facet, as discussed above. This is a computationally very expensive exercise, and is only worthwhile once the SKA array configuration has been finalised. For investigating and optimising array configurations it makes more sense to perform smaller scale simulations which still allow us to quantify the performance of the array.

We propose such a HI simulation here, which will partly match the co-moving volume of the HIPASS dataset. This requires a smaller number of individual simulation runs, and it is thus possible to re-run the simulation several times.

HIPASS is a blind HI radio survey of the sky at declinations southwards of 25 degrees. However to calculate the co-moving volume we use the initially presented catalogue covering the hole southern hemisphere. The sur-
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This survey covers a sky area of 21314 deg², a redshift range of z = 0.001–0.042 (corresponding to a co-moving volume of 0.013 Gpc³), and has a sensitivity limit approximately corresponding to a peak flux density of 0.05 Jy (see Zwaan et al. 2003 for a full description of the sample completeness). This survey yields a total number of 4315 sources, all of which are subsequently identified with optical galaxies (Doyle et al. 2005).

Using the SAX simulation to mimic the HIPASS survey no extrapolation of the sky simulation is needed because the simulated volume is large enough to cover the entire HIPASS volume. In fact this can be shown by comparing the HIPASS co-moving distance of 171 Mpc (z=0.042 and using the cosmological parameter of the Millennium simulation) which is smaller than the radius of the simulation box, i.e. 500/2 Mpc/h ∼ 342 Mpc.

Using the online query of the SAX simulation and defining the redshift and the sensitivity specifications of the HIPASS catalogue one obtain 4545 sources. This means that the SAX simulation predicts that the HIPASS catalog contains 4545 sources, which matches the observed number of 4315 sources within 5%. This difference can be partially attributed to the fact that HIPASS yields a continuously varying completeness function rather than a strict peak flux limit. Assuming no flux limits the SAX simulation predicts 772120 source within the HIPASS volume, i.e. 180-times more sources than picked up by HIPASS. However Table 1 shows the expected number counts assuming a minimum peak flux density of 3 µJy. The simulation still contain enough source to address e.g. the study of the faint end of the HI mass function and to make statistical significant predictions out to high cosmological distances.

Figure 5 shows the HI intensity map of an input cube. No continuum emission has been added and the individual galaxies are unresolved. The corresponding “observed sky” is shown in Fig. 6. In order to analyse these images the automated source finder, Duchamp, will be used to generate “observed” source catalogues for comparison to the input catalogues. An important part of this analysis will be to produce idealised input images with purely Gaussian noise of an equivalent level to cross-check the reliability and completeness of the source finding software in the presence of the image artifacts introduced by an interferometer.

3. Conclusions

A full e2e simulation path has been developed. The array simulator makes use of images or datacubes based on the S³ catalogues to simulate an observation. In the simulations no errors due to calibration or telescope hardware have been introduced, but a simplistic treatment of

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4 SAX query input: select count(*) from galaxies where zapparent between 0.001 and 0.042 and hiintflux*hilumpeak > 0.05

5 www.atnf.csiro.au/people/Matthew.Whiting/Duchamp
fuse emission by using the UV-gap (\(\Delta U\)) analysis techniques (Vir Lal et al. 2009) or by analysing the statistics of Fourier phases (Levrier et al. 2006).

The proposed HI simulations match the requirements for studying the capability of the SKA aperture array when imaging HI structures in nearby galaxies. Such simulations will also investigate the impact of different telescope designs on the proposed SKA blind HI surveys. The input HI sky will have an equivalent co-moving volume to that of the HIPASS survey, and this relatively small volume makes it feasible to re-run the simulations with different parameters within a reasonable time. With this setup we are able to analyse the “observed skies” and study the influence that the antenna layout has on a blind HI galaxy survey by investigating following points:

- completeness (peak flux density)
- positional accuracy
- redshift determination
- necessity of subtracting continuum emission and our ability to do so

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References

Alexander P., et al., 2007, SKA Memo, 93
de Oliveira-Costa A., Tegmark M., Gaensler B.M., Jonas J., Landecker T.L., Reich P., 2008, MNRAS, 388, 247
Doyle M.T., 2005, MNRAS, 361, 34
Holler C.M., Hills R.E., Jones M.E., Grainge K., Kaneko T., 2008, MNRAS, 384, 1207
Greisen E., 1990, Acquisition, Processing and Archiving of Astronomical Images, eds. Longo G. and Sedmak G., 125
Kettenis M., van Langevelde H.J., Reynolds C., Cotton B., 2006, ASPC, 351, 497
Levrier F., Falgarone E., Viallefond F., 2006, A&A, 456, 205
Obreschkow D., Croton D., DeLucia G., Khochfar S., Rawlings S., 2009a, ApJ, 698, 147
Obreschkow D., Rawlings S., 2009b, ApJ, 696, 129
Obreschkow D., Klöckner H.-R., Heywood I., Levrier F., Rawlings S., 2009c, ApJ, 703, 1890
Santos M., Amblard A., Pritchard J., et al., 2008, ApJ, 689, 1
Springel V., White S.D.M., Jenkins A., et al., 2005, Nature, 435, 629
Vir Lal D., Lebanov A.P., Jimenez-Monferrer S., 2009, SKA Memo, 107
Wilman R.J., et al., 2008, MNRAS, 388, 1335
Wilman R.J., Jarvis M.J., Mauch T., Rawlings S., Hickey S., 2010, MNRAS, submitted
Wrobel J.M. and Walker R.C., 1999, Synthesis Imaging in Radio Astronomy II, ASP Conference Series, 180, 171
Zwaan M.A., et al., 2003, AJ, 125, 2842
Zwaan M.A., Meyer M.J., Stavely-Smith L., Webster R.L., 2005, MNRAS, 359, L30