The Algorithmic Automation Problem: Prediction, Triage, and Human Effort

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Abstract

In a wide array of areas, algorithms are matching and surpassing the performance of human experts, leading to consideration of the roles of human judgment and algorithmic prediction in these domains. The discussion around these developments, however, has implicitly equated the specific task of prediction with the general task of automation. We argue here that automation is broader than just a comparison of human versus algorithmic performance on a task; it also involves the decision of which instances of the task to give to the algorithm in the first place. We develop a general framework that poses this latter decision as an optimization problem, and we show how basic heuristics for this optimization problem can lead to performance gains even on heavily-studied applications of AI in medicine. Our framework also serves to highlight how effective automation depends crucially on estimating both algorithmic and human error on an instance-by-instance basis, and our results show how improvements in these error estimation problems can yield significant gains for automation as well.

1 Introduction

On a variety of high-stakes tasks, machine learning algorithms are on the threshold of doing what human experts do with such high fidelity that we are contemplating using their predictions as a substitute for human output. For example, convolutional neural networks are close to diagnosing pneumonia from chest X-rays better than radiologists can \cite{14, 15}; examples like these underpin much of the widespread discussion of algorithmic automation in these tasks.

In assessing the potential for algorithms, however, the community has implicitly equated the specific task of prediction with the general task of automation. We argue here that this implicit correspondence misses key aspects of the automation problem; a broader conceptualization of automation can lead directly to concrete benefits in some of the key application areas where this process is unfolding.

We start from the premise that automation is more than just the replacement of human effort on a task; it is also the meta-decision of which instances of the task to automate. And it is here that algorithms distinguish themselves from earlier technology used for automation, because they can actively take part in this decision of what to automate. But as currently constructed, they are not set up to help with this second part of the problem. The automation problem, then, should involve an algorithm that on any given instance both (i) produces a prediction output; and (ii) additionally also produces a triage judgment of its effectiveness relative to the human effort it would replace on that instance.

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Viewed in this light, machine learning algorithms as currently constructed only solve the first problem; they do not pose or solve the second problem. In effect, currently when we contemplate automation using these algorithms, we are implicitly assuming that we will automate all instances or none. In this paper, we argue that when algorithms are built to solve both problems – prediction and triage – overall performance is significantly higher. In fact, even on tasks where the algorithm significantly outperforms humans on average per instance, the optimal solution is to automate only a fraction of the instances and to optimally divide up the available human effort on the remaining ones. And correspondingly, even on tasks where an algorithm does not beat human experts, the optimal solution may still be to automate a subset of instances.

Now is the right time to ask these questions because the AI community is on the verge of translating some of its most successful algorithms into clinical practice. Notably, an influential line of work showed how a well-constructed convolutional net trained on gold-standard consensus labels for diagnosing diabetic retinopathy (DR) outperforms ophthalmologists in aggregate, and these results have led to considerable optimism about the role of algorithms in this setting [15]. But the community’s discussion around these prospects has focused on the algorithms’ per-instance prediction performance without considering the problem of recognizing which instances to automate.

Using largely the same data, we build this additional, crucial component and find that, even in this context where an algorithm outperforms human experts in the aggregate, the optimal level of triage is not full automation. Instead significantly more accuracy can be had by triaging a fraction of the instances to the algorithm and leaving the remaining fraction to the human experts. Specifically, full automation reduces the error rate from roughly 5.5% by human doctors to 4% with an algorithm solving every instance; automation with optimal triage, though, reduces the error further to roughly 3.5% – effectively adding a significant further fraction to the gains that were realized by algorithmically automating the task in the first place.

This gain occurs for two reasons: first the algorithm’s high average performance hides significant heterogeneity in performance. For example, on roughly 40% of the instances the algorithm has zero errors. By the same token, on a small set of instances, the algorithm makes far more errors than average and these instances can be assigned to humans. Second, when the algorithm automates a fraction of the cases, that frees up human effort; reallocating that effort to the remaining cases can achieve further gains. In principle these gains could come from a single doctor spending additional time on the instance, or from multiple doctors looking at it; in our case, the available data allows us to explicitly quantify the gains arising from the second of these effects, due to the fact that we have multiple doctor judgments on each instance.

These results empirically demonstrate the importance of the triage component for the automation problem. We show that the gains we demonstrate are unlikely to have fully tapped the potential gains to be had through algorithmic triage: this neglected component deserves the kind of sustained effort from the machine learning community that the prediction component has received to date. In fact, given the disparity in efforts on these two problems, it is possible that the highest return to improving automation performance is through solving triage rather than further improving prediction.

2 General Framework

In a typical application where we consider using algorithmic effort in place of human effort, the goal is to label a set of instances of the problem with a positive or a negative label. For example, in a medical diagnosis setting, we may have a set of medical images, and the goal is to label each with a binary yes/no diagnosis. Let $x$ be an instance of the labeling problem, and let $a(x)$ be its ground truth value. For our purposes (as in the example of a binary diagnosis), we will think of this ground truth value as taking a value of either 0 or 1, with $a(x) = 0$ corresponding to a negative label and $a(x) = 1$ corresponding to a positive label.

How do we approach this problem algorithmically? Given a set $U$ of instances, we could train an algorithm to produce a numerical estimate $m(x) \in [0, 1]$ with the goal of minimizing a loss function $\sum_{x \in U} L(a(x), m(x))$, where $L(\cdot, \cdot)$ increases with the distance between its two inputs. For notational convenience, we will write $g(x)$ for $L(a(x), m(x))$, the algorithmic error on instance $x$. The $m(x)$ values are then converted into (binary) predictions, and we can evaluate the resulting error relative to ground truth. As a concrete example, one option is to threshold the $m(x)$ to produce a 0 or 1 value, and evaluate agreement with $a(x)$. 

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When a social planner considers the prospect of introducing algorithms into an existing task, we often imagine the question to be the following. The planner currently has human effort being devoted to instances of the task; for an instance \( x \in U \), we can imagine that there is a human output \( h(x) \), resulting in a loss \( f(x) = L(a(x), h(x)) \). The question of whether to automate the task could then be viewed as a comparison between \( \sum_{x \in U} g(x) \) and \( \sum_{x \in U} f(x) \) — the loss from algorithmic effort relative to the loss from human effort.

### Allocating Human Effort
In order to think about the activity of automation in a richer sense, it is useful to start from the realization that even in the absence of algorithms, the social planner is implicitly working with a larger space of choices than the simple picture above suggests. In particular, they have some available budget of total human effort, and they do not need to allocate it uniformly across instances: for an instance \( x \), the planner can allocate \( k \) units of human effort for different possible values of \( k \). There are multiple possible interpretations for the meaning of \( k \); for example, in the case of diagnosis we could think of \( k \) as corresponding to the number of distinct doctors who look at the instance, or alternately to the total amount of time spent collectively by doctors on the instance. Thus, our functions \( h \) and \( f \) should more properly be written as two-variable functions that take an instance \( x \) and a level of effort \( k \); we say that \( h(x,k) \) is the label provided as a result of \( k \) units of human effort on instance \( x \), and \( f(x,k) = L(a(x), h(x,k)) \) is the resulting loss that we would like to minimize.

Note that as functions of effort \( k \), it may be that \( f(x,k) \) and \( f(x',k) \) are quite different for different instances \( x \) and \( x' \). For example, instance \( x \) may be much harder than instance \( x' \), and hence \( f(x,k) \) will be much larger than \( f(x',k) \); similarly, instance \( x \) might not exhibit as much marginal benefit from additional effort as instance \( x' \), and hence the growth of \( f(x,k) \) over increasing values of \( k \) might be much flatter than the growth of \( f(x',k) \). The social planner might well not have precise quantitative estimates for values like \( f(x,k) \), but implicitly they are seeking to allocate human effort across the set of instances \( U \) so as to minimize the total loss incurred. And indeed, a number of basic protocols — such as asking for second opinions — can be viewed as increasing the amount of effort spent on instances where there might be benefits for error reduction.

### 2.1 Automation involving Algorithms and Humans

When algorithms are introduced, the social planner has several new considerations to take into account. First, the full automation problem should be viewed more broadly than just a binary comparison of human and algorithmic performance; it can involve decisions about the allocation of both human and algorithmic effort. The introduction of the algorithm need not be all-or-nothing: we can choose to apply it to some instances in such an instance human effort that we can allocate, and we decide to allocate on the remaining instances on which no human effort will be used (only the algorithm), and we will then optimally allocate human effort.

The general problem can therefore be viewed as follows. We would like to select a subset \( S \) of instances on which no human effort will be used (only the algorithm), and we will then optimally allocate human effort on the remaining instances \( T = U - S \). Suppose that we have a budget \( B \) on the total number of units of human effort that we can allocate, and we decide to allocate \( k_x \) units of effort to each instance \( x \in T \). On such an instance \( x \), we incur a loss of \( f(x,k_x) \), using our notation above; and on the instances \( x \in S \) we incur a loss of \( g(x) \) from the algorithmic prediction.

We thus have the following optimization problem.

\[
\begin{align*}
\text{Min} & \quad \sum_{x \in S} g(x) + \sum_{x \in T} f(x,k_x) \\
\text{subject to} & \quad \sum_{x \in T} k_x \leq B \\
& \quad S \cup T = U; \quad S \cap T = \emptyset
\end{align*}
\]

(1)

(2)

(3)
Our earlier discussions about algorithms and humans in isolation are special cases of this optimization problem: *full automation*, when the algorithm substitutes completely for human effort, is the case in which \( S = U \); and the social planner’s problem in the absence of an algorithm — which still involves decisions about the effort variables \( k_x \) — is the case in which \( T = U \). Intermediate solutions can be viewed as performing a kind of *triage*, a term we use here in a general sense for a process in which some instances go purely to an algorithm and others receive human attention.

By deliberately adopting a very general formulation, we can also get a clearer picture of the kinds of information we would need in order to perform automation more effectively. Specifically,

(i) In addition to making algorithmic predictions \( m(x) \), the automation problem benefits from more accurate estimates of the algorithm’s instance-specific error rate \( g(x) \).

(ii) The allocation of human effort benefits from better models of human error rate, including error as a function of effort spent \( f(x, k) \). As noted above, we can use an algorithm to help in estimating this human error rate.

(iii) Given estimates for the functions \( f \) and \( g \), we can obtain further performance improvements purely through better allocations of human effort in the optimization problem (1).

We note that the notion of human error involves an additional set of complex design choices, which is how humans decide to make use of algorithmic assistance on the instances (in the set \( T \)) where they spend effort. In particular, if we imagine that algorithmic predictions are available on the instances in \( T \), then the humans involved in the decision on \( x \in T \) may have the ability to incorporate the algorithmic prediction \( m(x) \) into their overall output \( h(x, k_x) \), and this will have an effect on the error rate \( f(x, k_x) \). In general, of course, it will be difficult to model a priori how this synthesis will work, although it is a very interesting question; we show that our results for the automation problem do not require assumptions about this aspect of the process, but we explore this question later in the paper.

### 2.2 Heuristics for Automation

If we think of the social planner as the entity tasked with solving the automation problem in (1), they are now faced with a set of considerations: not simply the binary question of whether to use human or algorithmic effort, but instead how to divide the instances between those (in \( S \)) that will be fully automated and those (in \( T \)) that will involve human effort, and how to estimate the error rates \( g(x) \) and \( f(x, k) \) so as to solve the allocation problem effectively.

We will show that significant performance gains can be achieved over both algorithmic and human effort even if we use only very simple heuristics for the different components of the allocation problem. Moreover, through a stronger benchmark based on ground truth, we will also show that much stronger gains are in principle achievable with improved approaches to the components.

We can describe the simplest level of heuristics in terms of sub-problems (i), (ii), and (iii) from earlier in this section. The simplest heuristic for (i) is to use the functional form of the variance, \( m(x)(1 - m(x)) \) as a measure of the algorithm’s uncertainty in its prediction on \( x \). A comparably natural predictor does not exist for (ii). We therefore design new algorithmic predictors to estimate the values of both (i) and (ii), and use these to guide the allocation of algorithmic and human effort. We show that using separate predictors in this way also strengthens the performance gains relative to the simpler heuristic based on \( m(x)(1 - m(x)) \), although even this basic heuristic yields improvements over full automation.

Given these predictors for (i) and (ii), what does this suggest about simple strategies for approximating (iii), the allocation of human effort? First, we could restrict attention to solutions in which each instance in \( T \) receives the same amount of effort. Thus, if there are \( N \) total instances in \( U \), we could choose a real number \( \alpha \in [0, 1] \), perform full automation on a set \( S \) of \( \alpha N \) instances, and divide the \( B \) units of human effort evenly across the remaining \( \beta = 1 - \alpha \) fraction of the instances. This means that each instance in the set receiving human effort gets \( B/\beta N \) units of effort. For simplicity, let us write \( B = cN \), so that the human effort per instance in this remaining set is \( c/\beta \). With this allocation of effort, the resulting loss is \( \sum_{x \in S} g(x) + \sum_{x \in T} f(x, c/\beta) \).
This restriction on the set of possible solutions suggests the following heuristic. Consider any partition of the instances into $S$ and $T$, and suppose we use the algorithm on all the instances. Then we can write the resulting loss in the following convenient way: $\sum_{x \in S} g(x) + \sum_{x \in T} g(x)$. Subtracting from the loss that results when we assign $c/\beta$ units of human effort to each instance in $T$, we see that the difference is $\sum_{x \in T} [f(x, c/\beta) - g(x)]$.

Thus, for a given value of $\alpha$ (specifying the fraction of instances that we wish to assign to the algorithm), it is sufficient to rank all instances $x \in U$ by $\tau_\alpha(x) = f(x, c/\beta) - g(x)$, and then choose the $\alpha N$ instances with the largest values of $\tau_\alpha$ to put in the set $S$ that we give to the algorithm. We can thus think of $\tau_\alpha(x)$ as the triage score of instance $x$, since it tells us the effect of algorithmic triage relative to human effort on the expected error.

2.3 Overview of Results

We put these ideas together in the context of a widely studied medical application, concerned with the diagnosis of diabetic retinopathy, detailed in the next section. We rank instances by their triage score, using simple forms for the algorithmic loss $g(x)$ and human loss $f(x, c/\beta)$, and we then search over possible values of $\alpha$, evaluating the performance at each. We find that there is range of values of $\alpha$, and a way of choosing $\alpha N$ instances to give to the algorithm, so that the resulting performance exceeds either of the binary choices of fully assigning the instances to the algorithm or to human effort.

As a scoping exercise, to see how strong the possible gains from our automation approach might be, we consider what would happen if we ranked instances by a triage score derived from a ground-truth estimate of the individual human error on each instance. Such a benchmark indicates the power of the optimization framework if we are able to get better approximations to the key quantities of interest — the functions $f$ and $g$. We find large performance gains from this benchmark, and we also explore some stronger methods to work on closing the gap between our simple heuristics and this ideal.

Different Costs for Error. In many settings, a social planner may associate higher costs to errors committed by automated methods relative to errors committed by humans — for example, there may be concern about the difficulty in identifying and correcting errors through automation, or the end users of the results may have a preference for human output. It is natural, therefore, to consider a version of the optimization problem in which the objective (1) has an additional parameter $\lambda$ specifying the relative cost of error between algorithms and humans. This new objective function is

$$\lambda \sum_{x \in S} g(x) + \sum_{x \in T} f(x, k_x). \quad (4)$$

One might suppose that as $\lambda$ grows large, the social planner would tend to favor purely human effort, given the relative cost of errors from automation. And indeed, the basic comparison that is typically made between $\sum_{x \in U} g(x)$ (for full automation) and $\sum_{x \in U} f(x, k_x)$ (for purely human effort) would suggest that this should be the case, since eventually $\lambda$ will exceed the ratio between these two quantities. But our more detailed framework makes clear that these aggregate measures of performance can obscure large levels of variability in difficulty across instances. And what we find in our application is that it is possible for the algorithm to identify a large set of instances $S$ on which it makes zero errors. Thus, even with strong preferences for human effort over algorithmic effort, it may still be possible to find sizeable subsets of the problem that should nevertheless be automated — a fact that is hidden by comparisons based purely on aggregate measures of performance.

3 Medical Preliminaries, Data and Experimental Setup

We first outline the details of the medical prediction problems, and describe the data and experimental setup used to design the automated decision making algorithm. As our primary goal is to study the interaction of
Figure 1: Example fundus photographs. Fundus photographs are images of the back of the eye, which can be used by an ophthalmologist to diagnose patients with different kinds of eye diseases. One common such eye disease is Diabetic Retinopathy, where high blood sugar levels cause damage to blood vessels in the eye.

In the mechanics of training our classifier, it will be useful to view DR diagnosis as a 5-class classification, using the 5-point grading scheme. However, when we consider the problem of triage and automation at a higher level, we will treat the task as a binary classification problem into images that are referable or non-referable.
Figure 2: **Diagram of Algorithm for Diagnosing Diabetic Retinopathy (DR).** The algorithm takes as input a fundus photograph, which, with doctor grades as targets, is used to train a convolutional neural network to perform 5-class classification of DR. For evaluation on an image \( i \) the output values of the convolutional neural network on grades \( \geq 3 \), \( o_3, o_4, o_5 \), are summed to give \( m(x_i) \), the total output mass on a referable diagnosis. \( m(x_i) \) is then thresholded with \( q_R \) – the threshold for a referable diagnosis. This binary decision is output by the algorithm.

The choice of the threshold \( q_R \) is made so that the total number of cases marked as referable by the algorithm matches the total number of cases marked as referable when aggregating the human doctor grades. This ensures that the effort, resources, and expense needed to act upon the algorithmic decisions match the current (feasible) effort resulting from the human decision making process. This is discussed in further detail in Section 3.4.

The result of this process is an algorithm taking as input a patient’s fundus photograph, and outputting a binary 0/1 decision on whether the patient has non-referable/referable Diabetic Retinopathy. We illustrate the components of the DR algorithm in Figure 2. The full details of our algorithm development setup can be found in Appendix Section A.

### 3.3 Evaluation

We evaluate our decision-making algorithm on a special, gold-standard *adjudicated* dataset [10]. This dataset is much smaller than our training data, but is meticulously labelled. For every fundus photograph in the dataset, there are many individual doctor grades, and also a single *adjudicated* grade, given after multiple doctors discuss the appropriate diagnosis for the image. This adjudicated grade acts as a proxy for the ground truth condition, and we use it to evaluate both the individual human doctors and the decision making algorithm. In Appendix Section A we carry out an additional evaluation of the methods on a different dataset, which exhibits the same results.

### 3.4 Aggregation and Thresholding

During evaluation and the triage process, we often have multiple (binary) grades per image. These grades might correspond to multiple different human doctors individually diagnosing the image, or the algorithm’s binary decision along with human doctor grades. In all of these cases, for evaluation, we must typically aggregate these multiple grades into a concrete decision – a single summary binary grade. To do so, we compute the mean grade and threshold by a value \( R \). If the mean is greater than \( R \), this corresponds to a decision of 1 (referable); otherwise the decision is 0 (non-referable).

The choice of the threshold \( R \) also affects the choice of \( q_R \) which is used for the algorithm’s decision. To compute \( q_R \), we first aggregate the multiple doctor grades per image into a single grade by computing their
mean and thresholding with $R$. This gives us the total number of patients marked as referable by the human doctors, and we pick $q_R$ so that the algorithm matches this number.

In the main text, we give results for $R = 0.5$, which corresponds to the majority vote of the multiple grades for an image. In the Appendix, we include results for $R = 0.3, 0.4$, which support the same conclusions.

4 The Triage Problem and Human Effort Reallocation

The performance of human experts and algorithmic decisions are typically summarized and compared via a single number, such as average error, F1 score, or AUC. Seeing the algorithm outperform human experts according to these metrics might suggest the hypothesis that the algorithm uniformly outperforms human experts on any given instance.

What we find instead, however, is significant diversity across instances in the performance of humans and algorithms: for natural definitions of human and algorithmic error probability (formalized below), there are instances in which human effort has lower error probability than the algorithm, and instances in which the algorithm has lower error probability than human effort. Moreover, this diversity is partially predictable: we can identify with non-trivial accuracy those instances on which one entity or the other will do better. This diversity and its predictability is an important component of the automation framework, since it makes it possible to divide instances between algorithms and humans so that each party is working on those instances that are best suited to it.

We first study this performance diversity, and then move on to the problem of allocating effort between humans and algorithms across instances.

4.1 Per Instance Error Diversity of Humans and Algorithms

In order to look at the differences in performance between humans and algorithms on an instance-by-instance level, we want to define, for each instance $x_i$ in the adjudicated dataset, an error probability $\Pr[H_i]$ for the doctors (human experts) and an error probability $\Pr[M_i]$ for the algorithm.
The quantity $\Pr[H_i]$ is straightforward to compute on the adjudicated dataset: for an instance $x_i$, suppose that $n_i$ doctors evaluate it, assigning it binary non-referable/referable grades $h^{(1)}(x_i), ..., h^{(n_i)}(x_i)$. Let $a(x_i)$ be the binary adjudicated grade for $x_i$. Then we can define

$$\Pr[H_i] = \frac{1}{n_i} \sum_{j=1}^{n_i} |h^{(j)}(x_i) - a(x_i)|.$$ 

That is, $\Pr[H_i]$ is the average disagreement of doctors with the adjudicated grade.

Computing $\Pr[M_i]$ is a little more complicated. Recall that for an instance $i$, the convolutional neural network model in the algorithm outputs a value $m(x_i)$ between $[0, 1]$ that is then thresholded to give a binary decision. A naive estimate of the error probability could therefore be $m(x_i)$ if the instance is not referable, and $1 - m(x_i)$ if the instance is referable. Unfortunately, deep neural networks are well-known to be poorly calibrated [5], and this naive approximation is both poorly calibrated and at a different scaling to the human doctors. This is not a concern for the algorithm’s binary decision, since only the rank-ordering of the $m(x_i)$ values matter for this, but it poses a challenge for producing a probability that can serve as $\Pr[M_i]$.

4.1.1 Determining Algorithm Error Probabilities

To overcome this issue, we develop a simple method to calibrate the convolutional neural network’s output. Recall that the neural network outputs a value $m(x_i) \in [0, 1]$ for each image $x_i$—i.e., it induces a ranking over the images $x_i$, which is used to determine the algorithmic decision. We evaluate this induced ranking directly by asking:

'Suppose we produced a (random) number $R$ of referable instances by sampling a random doctor for each instance, what is the probability that $x_i$ is among the top $R$ instances in the induced ranking?'

We define $\tilde{p}(x_i)$ as the probability that the prediction algorithm declares $x_i$ to be referable. We can then define the error probability, $\Pr[M_i]$, as $\tilde{p}(x_i)$ if the adjudicated grade $a(x_i)$ is referable, and $1 - \tilde{p}(x_i)$ if $a(x_i)$ is non-referable. In Appendix Section [8] we provide specific details of the implementation.

4.1.2 Results on Performance Diversity

We can now use the estimate of $\Pr[M_i]$ and $\Pr[H_i]$ to study the variation in human expert and algorithmic error across different instances. Specifically, we plot a histogram of values of $\Pr[H_i] - \Pr[M_i]$ across all the adjudicated image instances.

The result is shown in Figure [3]. We see that while there are more images where $\Pr[M_i] < \Pr[H_i]$, there is a non-trivial fraction of images with $\Pr[M_i] > \Pr[H_i]$. In the subsequent sections, we analyze different ways of predicting these differences as a way to perform triage, and demonstrate the resulting gains.

4.2 Performing Triage and Reallocating Human Effort

In formulating the basic problem of automation, we considered two baselines for performance. The first is full automation, in which the overall loss is $\sum_{x_i \in U} g(x_i)$. The second is equal coverage of all instances by human effort: if we have a budget of $B = cn$ units of effort for $N$ instances, then allocate $c$ units of human effort to each, resulting in a loss of $\sum_{x_i \in U} f(x_i, c)$. Our goal here is to show that by allocating human and algorithmic effort more effectively according to optimization problem [1] from Section 2 we can improve on both of these baselines.

Recall the basic heuristic from Section 2 for an arbitrary $\alpha \in [0, 1]$, we compute a triage score $\tau_\alpha(x_i)$ for each instance $x_i$; we assign the first $\alpha N$ to the set $S$ to be handled by the algorithm, and we allocate equal amounts of human effort to the remaining set $T$ of $(1 - \alpha)N$ instances. Note that $\alpha = 1$ corresponds to the full automation baseline, while $\alpha = 0$ corresponds to equal coverage of all instances by human effort. We will see, however, that stronger performance can be achieved for intermediate values of $\alpha$.

We begin with two ways of computing the triage score. The first follows the basic strategy from Section 2 where we train two algorithmic predictors to estimate (i) the algorithm’s error probability, $\Pr[M_i]$ and (ii) the human error probability $\Pr[H_i]$. Specifically, we train two auxiliary neural networks, one to predict
Pr \([H_i]\) and one to predict Pr \([M_i]\). To predict Pr \([H_i]\), we build off of the work of \cite{13} on direct prediction of doctor disagreement: we label each example with a 0 if there is agreement amongst the doctor grades, and 1 otherwise, and train a small neural network to predict these agreement labels from the image embedding. A similar setup is employed for predicting Pr \([M_i]\), where the binary label now corresponds to whether the output of the diagnostic 5-class convolutional neural network agrees with the doctor grades – i.e. does the model make an error on that image. The full details of this process are described in Appendix \cite{13}.

The second method of computing a triage score establishes an “ideal” benchmark on the potential power of the optimization problem \eqref{equation:optimization} using aspects of ground truth, sorting the instances by the true value of Pr \([H_i] - Pr \([M_i]\), since this divides the instances between humans and algorithms based on the relative strength of each party on the respective instances.

In both cases, we determine the performance of the human effort using the average of a corresponding number of randomly sampled doctor grades from the data. This allows us to demonstrate improvements without any assumptions on how the doctors might use information from the algorithmic predictions on these instances. It is also reasonable, however, to imagine a scenario in which the algorithmic predictions are still freely available even on the instances that we assign to the human doctors, and to consider simple models for how the doctor grades might be combined with these algorithmic predictions. We consider this case in the Appendix, which supports the same conclusions.

4.2.1 Triage Results

The results for these two triage scores, as we vary \(\alpha\), are shown in Figure \ref{fig:triage_results}. The figure depicts both the average error (bottom row), as well as the F1 score (top row), which accounts for imbalances between the number of referable and non-referable instances. The left column corresponds to using the difference between the predicted values of Pr \([H_i]\) and Pr \([M_i]\) as a triage score, while the right column corresponds to using the true value Pr \([H_i] - Pr \([M_i]\) to perform triage. In both triage schemes, we observe that the best performance comes for \(0 < \alpha < 1\), beating both the full automation protocol (dotted black line) and equal coverage of all instances by human effort (coloured dotted lines).

While combining algorithmic and human effort in both of these ways leads to performance gains, we see that the ground truth triage ordering performs significantly better than triaging by the predicted error probability. This suggests that learning better triage predictors might have an even greater impact on overall deployed performance than continuous slight improvements to diagnostic accuracy.

4.2.2 The Simplest Heuristic: Algorithmic Uncertainty

In the previous section, we saw the results of training two separate algorithmic predictors to estimate the values of Pr \([H_i]\) and Pr \([M_i]\), and using the difference between these predicted values as a triage score. An even simpler triage score is given by only using the algorithm’s uncertainty, \(m(x)(1 - m(x))\). In Figure \ref{fig:algorithmic_uncertainty}, we show that even this triage score, available ‘for free’ from the algorithmic predictor, improves upon pure automation and pure human effort, although larger gains are available through using the two algorithmic error predictors. These results reiterate the rich possibilities for gains from algorithmic triage.

4.3 Differential Costs and Zero-Error Subsets

Finally, we recall a further consideration from the framework in Section \ref{sec:framework} suppose the social planner views errors made by algorithms as more costly than errors made by humans, resulting in an objective function of the form in \eqref{equation:objective}, \(\lambda \sum_{x \in S} g(x) + \sum_{x \in T} f(x, k_x)\). As \(\lambda\) becomes large, what does this imply about the use of algorithmic predictions?

We find in our application that it is possible to identify large subsets of the data on which the algorithm achieves zero error. Such a fact can easily be hidden by considering only aggregate measures of algorithmic performance, and it implies that even when \(\lambda\) is large, there may still be an important role for algorithms in automation.
Figure 4: Combining algorithmic and human effort by triaging outperforms full automation and the equal coverage human baseline. Left column: triage by the difference between the predicted values of $\Pr[H_i]$ and $\Pr[M_i]$. Right column: triage by ground truth $\Pr[H_i] - \Pr[M_i]$ We order the images by their triage scores (predicted $\Pr[H_i] - \Pr[M_i]$ for the left column and ground truth $\Pr[H_i] - \Pr[M_i]$ on the right), and automate an $\alpha$ fraction of them. The remaining $(1 - \alpha)N$ images have the human doctor budget ($N, 2N, 3N$ grades) allocated amongst them, according to the equal coverage protocol. This is described in further detail in Appendix Section C. The black dotted line is the performance of full automation, and the coloured dotted lines the performance of equal coverage for the different total number of doctor grades available. We see that triaging and combining algorithmic and human effort performs better than all of these baselines. Triaging by ground truth (right column) gives significant gains, and suggests that better triage prediction is a crucial problem that merits further study. In Appendix Section D we also include results when the remaining $(1 - \alpha)N$ cases have the algorithm grade available, along with the reallocated human effort. The qualitative conclusions are identical.
Figure 5: **Even triaging by algorithm uncertainty leads to gains over pure algorithmic and pure human performance.** Instead of the separate error prediction algorithms, we triage by the simple algorithm uncertainty: \( m(x)(1 - m(x)) \), which acts as a proxy for algorithm error probability (and no explicit modelling of human error probability.) The same qualitative conclusions hold with this simple triage score also (purple line), although larger gains are achieved with the separate error prediction algorithms (blue line). These results are for \( N \) doctor grades, the same conclusions hold for \( 2N \), \( 3N \) grades.

To quantify this effect, we order the instances by a triage score as in our earlier analyses. We then look at the average error of the algorithmic predictions on the first \( \alpha \) fraction of images: for \( \alpha \) varying between 0 and 1, we plot \( M_{err}(\alpha N) \)

\[
\frac{M_{err}(\alpha N)}{N}
\]

where \( M_{err}(\alpha N) \) is the number of errors made by the model on the first \( \alpha N \) instances.

### 4.3.1 Results

Figure 6 left pane shows the results of plotting this quantity. We triage the cases both by our prediction of \( \Pr[H_i] - \Pr[M_i] \) from the two error prediction algorithms as well as the simple algorithm uncertainty term, \( m(x)(1 - m(x)) \). We evaluate the average error of the algorithmic predictions on the first \( \alpha \) fraction of images, over three repetitions of training the diagnostic neural network component of the algorithm. We see that even using the simple \( m9x)(1 - m(x)) \) as a triage score, we can identify a zero-error subset that is 35% the size of the entire dataset. Similar to Section 4.2.2, further improvements are shown by predicting the value of \( \Pr[H_i] - \Pr[M_i] \). The right pane of Figure 6 shows this result, where we can identify a zero-error subset of size 44%, again averaged over three repetitions.

### 5 Related Work

With the successes of machine learning and particularly deep learning methodologies in modalities such as imaging, there have been numerous works comparing algorithmic performance to human performance in medical tasks, albeit in frameworks that implicitly interpret automation as success in prediction. In this prediction setting, the general comparison is between the case in which only the algorithm is used and the case in which only human effort is used; such comparisons have been done for chest x-rays [14], for Alzheimer’s detection from PET scans [6], and for the setting we consider here based on diabetic retinopathy
Figure 6: Triage identifies large subsets of the data with zero error. We plot the average cumulative error $M_{err}(\alpha N)$, where $M_{err}(\alpha N)$ is the number of errors made by the algorithm on the first $\alpha$ fraction of the $N$ images when triaged. We observe that triaging even by the simple uncertainty measure, $m(x_i)(1 - m(x_i))$ (left plot), can identify a 35% fraction of data where the algorithm makes zero errors. Using the separate error prediction model from Section 4.2.2 we can improve on this, identifying 44% of the data where the algorithm has zero errors. The plot is averaged over three repetitions (so each repeat identified at least 35%, 44% of the data respectively.)

diagnosis from fundus photographs (and OCT scans) [4, 7]. The recent survey paper by Topol [15] references several additional studies of this kind. A few papers have begun to look at fixed modes of interaction with humans, including processes in which algorithmic outputs are reviewed by physicians [3, 5, 11], as well as fixed combinations of physician and algorithmic judgments [12].

6 Discussion

This work has presented a framework for analyzing automation by algorithms. Rather than treating the introduction of algorithms in an all-or-nothing fashion, we show that stronger performance can be obtained if algorithms are used both (i) for prediction on instances of the problem, and (ii) for providing triage judgments about which instances should be handled algorithmically and which should be handled by human effort. This broader formulation of the automation question highlights the importance of accurately estimating the propensity of both humans and algorithms to make errors on a per-instance basis, and the use of these estimates in an optimization framework for allocating effort efficiently. Analysis of an application in diabetic retinopathy diagnosis shows that this framework can lead to performance gains even for well-studied problems in AI applications in medicine.

Through the analysis of benchmarks for stronger performance, we also highlight how stronger predictions of per-instance error has the potential to yield still better performance. Our findings thus demonstrate how further study of algorithmic triage and its role in allocating human and computational effort has the potential to yield substantial benefits for the task of automation.

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[15] Eric Topol. High-performance medicine: the convergence of human and artificial intelligence. *Nature Medicine*, 25:44–56, 2019.
A Training Data and Models Details

Our training dataset consists of fundus photographs with labels corresponding to individual doctor grades. There are 5 possible DR grades and hence 5 possible class labels. A subset of this data has fundus photographs with more than one doctor grade, corresponding to multiple doctors individually and independently deciding on the grade for the image. The label for these images is not a one-hot class label but the empirical distribution of grades. For example, if an image \( i \) has grades \( \{2, 3, 3\} \), then its label would be \( [0, 1./3, 2./3, 0, 0] \).

On this data, we train a convolutional neural network, an Inception-v3 model with weights pretrained from ImageNet and a new five class classification head. We train with the Adam optimizer \([9]\) and an initial learning rate of 0.005. To better calibrate the model, we retrain the very top of the network (from the PreLogits layer) on just the data with two or more doctor grades.

Training Error Probability Prediction Models For Figures 4, 5 and 6, we use separate error probability prediction algorithms to predict the values of \( Pr[H_i] \) and \( Pr[M_i] \). The setup for predicting \( Pr[M_i] \) is as follows: after training the main convolutional neural network on the train dataset, we train a small fully connected deep neural network to take the prelogit embeddings of a train image \( x_i \), and predict whether or not the main convolutional neural network was correct on that image. The label for the image is binary: agree/disagree on whether the mass \( m(x_i) \) put on referable by the convolutional neural network thresholded at 0.5 equals the mass on referable by the human doctor grades, again thresholded at 0.5.

The setup for training \( Pr[H_i] \) builds off of \([13]\). First, we only select cases for which we have at least two doctor grades. For these, we take the image embedding from the Prelogit layer of the large diagnostic convolutional neural network as input, and the label as a binary target. This label is defined as follows: we split the available doctor grades into two evenly sized sets \( A \) and \( B \). We aggregate all the grades in \( A \) into a single referable/non-referable grade by averaging and thresholding at 0.5, and do the same for the grades in \( B \). If these two aggregated grades agree, we label the image with 0 (agreement, low doctor error probability), if not, we label with 1 (disagreement, high doctor error probability).

B Computing \( Pr[M_i] \)

In Section \([4.1.1]\) we overviewed the method used to define a well calibrated error probability for the output of the convolutional neural network. In Algorithm \([\ ]\), we give a step-by-step overview of the implementation of this method. In our experiments, we set \( C = 2000 \).

C Triage and Allocation Algorithm

When using triage to reallocate human effort, we first order the instances by their triage scores, and then fully automate the first \( \alpha N \) of them. On the remainder \((1 - \alpha)N \) images, we allocate the budget of \( cN \) human doctor grades we have available. To allocate this set of \( cN \) grades, we use the equal coverage protocol: each of the remaining \((1 - \alpha)N \) cases gets \( cN/(1 - \alpha)N \) grades. If this is a non-integer amount, with \( r \) spare grades, the \( r \) cases identified as the hardest (according to the triage scores) get an additional grade. We then compute the final binary decision by taking the mean grade (for each case) and thresholding by 0.5 (the majority vote.)

C.1 Results on other Thresholds

As described in Section \([3.4]\) at evaluation, for an instance with multiple grades we aggregate all the scores by taking the mean and thresholding. In the main text, we pick this threshold to be 0.5, corresponding to the majority vote of all the grades. In Figure \([\ ]\), we show the results corresponding to Figure \([\ ]\) in the main text, but for when we take the thresholds to be 0.3 (top row) and 0.4 (bottom row). We see that the qualitative conclusions remain the same – combining human and algorithmic effort beats the full allocation and equal
Algorithm 1: Model Error Probability Calibration

1: $\text{Err}_i = 0$ for $i$ in instances.
2: for ($r = 0; r < C; r++)$ do \hspace{1cm} \triangleright C is a sufficiently large constant.
3: \hspace{1cm} $R = 0$
4: \hspace{1cm} for $i$ in instances do \hspace{1cm} \triangleright Sample a doctor grade and count number of referables.
5: \hspace{1cm} \hspace{1cm} Sample doctor grade $h^{(i)}$
6: \hspace{1cm} \hspace{1cm} if ($h^{(i)} \geq 3$) then
7: \hspace{1cm} \hspace{1cm} \hspace{1cm} $R \leftarrow R + 1$
8: \hspace{1cm} \hspace{1cm} end if
9: \hspace{1cm} end for
10: \hspace{1cm} Rank instances $i$ from highest to lowest $m(x_i)$
11: \hspace{1cm} $A_R = \{i: \text{rank}(i) \leq R\}$
12: \hspace{1cm} for $i$ in instances do \hspace{1cm} \triangleright Assign binary grades to instances. Top $R$ referable.
13: \hspace{1cm} \hspace{1cm} if ($i \in A_R$) then
14: \hspace{1cm} \hspace{1cm} \hspace{1cm} $m_i \leftarrow 1$
15: \hspace{1cm} \hspace{1cm} else
16: \hspace{1cm} \hspace{1cm} \hspace{1cm} $m_i \leftarrow 0$
17: \hspace{1cm} \hspace{1cm} end if
18: \hspace{1cm} $\text{Err}_i \leftarrow \text{Err}_i + |m_i - a_i|$ \hspace{1cm} \triangleright $a_i$ is the adjudicated grade
19: \hspace{1cm} end for
20: end for
21: return $\Pr[M_i] = \frac{\text{Err}_i}{C}$ \hspace{1cm} \triangleright Error probability by averaging over number of repetitions.

coverage protocols for both triage by the error prediction models and triage by the ground truth. We also see the same significant gap between ground truth and triage by error predictions.

Note that this choice of threshold affects the choice of $q_{R}$, which is chosen so that the number of cases marked as referable by the model matches the number of cases marked as referable by the aggregated and thresholded grade of the human doctors, and could potentially affect the results of Figure 6. However, as shown in Figure 8, the choice of aggregation threshold does not affect the identification of zero error subsets.

D Triage and Human Effort Reallocation with Model Grades

The triage process for effort reallocation – Figures 4, 11 – assumes that the algorithm decision is not available for the $(1 - \alpha)N$ cases that are not automated. This may be the situation if computing an algorithm decision is expensive (less likely) or (more likely) the algorithm decision is purposefully not shown in cases where it is unsure, so as not to bias the human doctors. However, another equally likely scenario is that the algorithm decision is also available ‘for free’ for the $(1 - \alpha)N$ cases that are not fully automated. In Figure 9, we show the effort reallocation results from triaging if the model grades were available for all the cases (compare to Figure 4 in the main text). We observe that all of the main conclusions – the optimal performance is through a combination of automation and human effort, which beats both full automation and the different equal coverage baselines.

E Results on Additional Holdout Dataset

The results in the main text are on the adjudicated evaluation dataset, which, aside from multiple independent grades by individual doctors, also have a consensus score, the adjudicated grade, which is used as a proxy for ground truth. To further validate our result, we use an additional holdout set which doesn’t have an adjudicated grade, but does have many individual doctor grades. For each instance $i$, we use half of its grades to compute a proxy ground truth grade, by aggregating and then thresholding the doctor grades. The other

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The threshold for referable after aggregating (averaging) the grades was 0.5 (a majority vote), and here we show the results if the threshold used was 0.3 (top row) or 0.4 (bottom row). We see that the same qualitative conclusions hold as in Figure 4.

The size of the zero error subsets remain the same, showing that the choice of threshold does not affect the identification of these subsets.

We assume that the algorithm’s grade is available for all the patient cases. We see that the same qualitative conclusions hold – a mix of automation and human effort outperforming the pure algorithm/human expert.
half of the grades are used in effort reallocation and evaluating the equal coverage baseline. The individual doctor grades in this dataset are slightly noisier (higher disagreement rates) than in the adjudicated evaluation dataset. Nevertheless this additional evaluation also supports all of the main findings.

The results on this dataset are qualitatively identical to those with the adjudicated data. Again, we see that there is a diverse spread of $\Pr[H_i] - \Pr[M_i]$ across instances, with around 10% of the instances having the human experts perform better (Figure 10).

This diversity continues to be predictable, and we observe that triaging (by the error prediction models and by the ground truth) to combine human expert effort and the algorithm’s decisions, Figure 11, also demonstrates that this combination works better than both full automation and equal coverage – the same conclusions seen in Figure 4 in the main text. Like the main text, we see a gap between triaging by the error prediction models and the ground truth score.

Finally, we also test to see if triaging can help find sets of zero error, like in Section E and Figure 6. We find that this is indeed the case, though the fractions are slightly smaller with this holdout dataset, likely because the labels are noisier than on the adjudicated evaluation dataset.

We also see that the fraction of zero error examples triaged is slightly lower with the separate error prediction model (Figure 12 right) than triaging by model uncertainty (Figure 12 left). The reason for this becomes apparent after further inspection: the results of Figure 12 are averaged over three independent repetitions of training a main diagnostic model, and a corresponding separate error model. We find that one of the three repetitions of the separate error model makes two errors – at 10% of the way through the data, it triages two examples that are errors. This causes the percentage with zero error to drop from 24% to 10%. If we account for these two errors, we see that in fact triaging by the error prediction model is doing comparably to triaging by algorithm uncertainty, where allowing two errors gets to 20% of the data.
Figure 11: Triaging to combine human effort and algorithm decisions outperforms full automation and the equal coverage protocols, compare to Figure 4 in the main text. We perform the same experiments as in Figure 4 in the main text, using the aggregated doctor grades as the ground truth instead of the adjudicated grade.
Figure 12: **Proportion of data with zero errors when triaging.** Compare to Figure 6 in the main text. The proportion of the dataset found with zero errors is slightly lower, likely because the labels are noisier, and total error is much higher (10% compared to 4% in the main text.) Unlike the main text, we see that triaging by algorithmic uncertainty, left pane, seems to perform better than triaging with a separate model. Upon closer inspection, we find that this is because one repetition of the separate error model makes two errors earlier on, and accounting for this (green dotted lines) shows that the separate error model performs comparably/slightly better.