Boundary Zonal Flow in Rotating Turbulent Rayleigh-Bénard Convection

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For rapidly rotating turbulent Rayleigh–Bénard convection in a slender cylindrical cell, experiments and direct numerical simulations reveal a boundary zonal flow (BZF) that replaces the classical large-scale circulation. The BZF is located near the vertical side wall and enables enhanced heat transport there. Although the azimuthal velocity of the BZF is cyclonic (in the rotating frame), the temperature is an anticyclonic traveling wave of mode one, whose signature is a bimodal temperature distribution near the radial boundary. The BZF width is found to scale like $Ra^{1/4}Ek^{3/4}$ where the Ekman number $Ek$ decreases with increasing rotation rate.

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Turbulent fluid motion driven by buoyancy and influenced by rotation is a common phenomenon in nature and is important in many industrial applications. In the widely studied laboratory realization of turbulent convection, Rayleigh-Bénard convection (RBC) [1,2], a fluid is confined in a convection cell with a heated bottom, cooled top, and adiabatic vertical walls. For these conditions, a large scale circulation (LSC) arises from cooperative plume motion and is an important feature of turbulent RBC [1]. The addition of rotation about a vertical axis produces a different type of convection as thermal plumes are transformed into thermal vortices, over some regions of parameter space, heat transport is enhanced by Ekman pumping [3–10], and statistical measures of vorticity and temperature fluctuations in the bulk are strongly influenced [11–17]. A crucial aspect of rotation is to suppress, for sufficiently rapid rotation rates, the LSC of nonrotating convection [12,13,18,19], although the diameter-to-height aspect ratio $\Gamma = D/H$ appears to play some role in the nature of the suppression [20].

In RBC geometries with $1/2 \leq \Gamma \leq 2$, the LSC usually spans the cell in a roll-like circulation of size $H$. For rotating convection, the intrinsic linear scale of separation of vortices is reduced with increasing rotation rate [21,22], suggesting that one might reduce the geometric aspect ratio, i.e., $\Gamma < 1$ while maintaining a large ratio of lateral cell size to linear scale [5]; such convection cells are being implemented in numerous new experiments [23]. Thus, an important question about rotating convection in slender cylindrical cells is whether there is a global circulation that substantially influences the internal state of the system and carries appreciable global heat transport. Direct numerical simulations (DNS) of rotating convection [24] in cylindrical geometry with $\Gamma = 1$, inverse Rossby number $1/Ro = 2.78$, Rayleigh number $Ra = 10^9$, and Prandtl number $Pr = 6.4$ ($Ro$, $Ra$, and $Pr$ defined below) revealed a cyclonic azimuthal velocity boundary-layer flow surrounding a core region of anticyclonic circulation and localized near the cylinder sidewall. The results were interpreted in the context of sidewall Stewartson layers driven by active Ekman layers at the top and bottom of the cell [25,26].

Here, we show, through DNS and experimental measurements for a cylindrical convection cell with $\Gamma = 1/2$ at large $Ra$ and for a range of rotation rates from slow to rapid,
that a wider (several times the Stewartson layer width) annular flow, denoted as boundary zonal flow (BZF), has profound effects on the overall flow structure and on the spatial distribution of heat flux. In particular, this cyclonic zonal flow surrounds an anticyclonic core. The BZF has alternating temperature sheets that produce bimodal temperature distributions for radial positions \( r/R > 0.7 \) and that contribute greatly to the overall heat transport; 60\% of heat transport are carried in the BZF. Although the location of the azimuthally averaged maximum cyclonic azimuthal velocity, the root-mean-square (rms) vertical velocity fluctuations, and the normalized vertical heat transport at the midplane are consistent with a linear description of a Stewartson-layer scaling [24], the dynamics of temperature, vertical velocity, and heat transport in the BZF are more complex and interesting. The robustness of the BZF state as evidenced by its existence over 7 orders of magnitude in \( Ra \) and experiment and over a range \( 1/2 \leq \Gamma \leq 2 \) and \( 0.1 \leq Pr \leq 4.4 \) (results to be presented elsewhere) suggests that this is a universal state of rotating convection that needs a physical understanding.

The dimensionless control parameters in rotating RBC are the Rayleigh number \( Ra = \alpha g \Delta H^3/(\kappa \nu) \), Prandtl number \( Pr = \nu/\kappa \), cell aspect ratio \( \Gamma \), and Rossby number \( Ro = \sqrt{\alpha g \Delta H/(2 \Omega H)} \) or, alternatively, Ekman number \( Ek = \nu/(2 \Omega H^2) \). Here, \( \alpha \) is isobaric thermal expansion coefficient, \( \nu \) kinematic viscosity, \( \kappa \) fluid thermal diffusivity, \( g \) acceleration of gravity, \( \Omega \) angular rotation rate, and \( \Delta \) temperature difference between the hotter bottom and colder top plates. The main integral response parameter we consider is the Nusselt number \( Nu = \langle \mathcal{F}_z \rangle_{t,V} \), where \( \langle \cdot \rangle_{t,V} \) denotes the time and volume averaging and \( \mathcal{F}_z \equiv [u_z (T - T_0) - \kappa \partial_z T]/(\kappa \Delta/H) \) is the normalized vertical heat flux with \( u_z \) being the vertical component of the velocity and \( T_0 \) the average of the top and bottom temperatures.

We present numerical and experimental results [27] for rotating RBC in a \( \Gamma = 1/2 \) cylindrical cell and \( 1/Ro = 0, 0.5, \) and 10. The DNS used the GOLDFISH code [28,29] with \( Pr = 0.8 \) and \( Ra = 10^9 \). The experiments used pressurized sulfur hexafluoride (SF\(_6\)) and were performed over a large parameter space in the High Pressure Convection Facility (HPCF, 2.24 m high) at the Max Planck Institute for Dynamics and Self-Organization in Göttingen [30]. In the studied parameter range, the Oberbeck–Boussinesq approximation is valid [31–33], and the centrifugal force is negligible [8,34,35].

First, we consider the azimuthal variation of the temperature measured by thermal probes at or near the sidewall, a commonly used technique for parametrizing the LSC in RBC [18,20,36–38]. We measured, experimentally and in corresponding DNS, the temperature at eight equidistantly spaced azimuthal locations of the sensors for each of three distances from the bottom plate: \( z/H = 1/4, 1/2, \) and \( 3/4 \). The probability density functions (PDFs) of the experimental data without rotation (\( 1/Ro = 0, Ra = 8 \times 10^{12} \)) in Fig. 1(a) show a distribution with a single peak and slight asymmetry to hotter (colder) fluctuations for heights smaller (larger) than \( z/H = 1/2 \), whereas the PDFs for rapid rotation (\( 1/Ro = 10, \) Fig. 1(b)), show a bimodal distribution that is well fit by the sum of two Gaussian distributions. The corresponding PDFs of the DNS data (at \( Ra = 10^6 \)) show the same qualitative transition from a single peak without rotation to a bimodal distribution in the rapidly rotating case with similar hot-cold asymmetry for different \( z \) [Figs. 1(c) and 1(d)]. To understand the nature of the emergence of a bimodal distribution near the radial boundary, we consider the DNS data in detail.

The LSC for nonrotating convection in cells with \( 1/2 \leq \Gamma \leq 2 \) and at large \( Ra \) extends throughout the entire cell with a large roll-like circulation [39]. With slow rotation, Coriolis forces induce anticyclonic motion close to the plates owing to the diverging flow between the LSC and the corner rolls. At the midplane, the LSC is tilted with a small inward radial velocity component that rotation spins up into cyclonic motion. These tendencies are illustrated for \( 1/Ro = 0.5 \) in Figs. 2(a) and 2(c), respectively, where streamlines of time-averaged velocity are overlaid on the field of azimuthal velocity. Figure 2(a) shows fields evaluated at the thermal boundary layer (BL) height \( z = \delta_0 = H/(2 Nu) \).
indicates anticyclonic (cyclonic) motion. In (d), locations \(\delta_\theta\) see Fig. 2(d). The core region, on the other hand, is strongly where cyclonic vorticity is concentrated at the midplane, increasing (decreasing) \(\delta_\theta\). (based on maximum of rms of \(u_z\)). \(\delta_{\text{rms}}\) was used to define the sidewall Stewartson layer thickness in rotating convection [24], and our results for \(\langle u_\phi \rangle_\text{rms}\) are consistent with that description. What was absolutely not expected is the strong azimuthal variation of the instantaneous temperature \(T\) shown in Fig. 3(c), a feature that defines the global flow circulation, namely, the spatial distribution of the heat transport which is the origin of the bimodal temperature distributions seen in the experiments and DNS.

The strong variations in instantaneous temperature shown in Fig. 3(c) organize into anticyclonic traveling waves illustrated in the angle-time plot of \(T\), Fig. 4(a). The BZF height is order \(H\), Fig. 3(c), but is increasingly localized in the radial direction as the rotation rate increases (\(Ro\) and \(Ek\) decrease) so that \(\delta_\theta/R \ll 1\). The azimuthal mode of \(T\) is highly correlated with a corresponding mode of the vertical velocity, Fig. 4(b), with a resulting coherent compensating Stewartson layers along the sidewalls with upflow from the bottom and downflow from the top [24,42]. This classical BL analysis was successfully applied to rotating convection [24] for a \(\Gamma = 1\) cylindrical cell with \(Pr = 6.4\) and \(10^6 \leq Ra \leq 10^{10}\) in both experiment and DNS. No evidence for a coherent large-scale circulation for rapid rotation was found in those studies.

For our conditions, \(Pr = 0.8\), \(Ra = 10^9\), and \(1/Ro = 10\), we compute the time- and azimuthal-average azimuthal velocity \(\langle u_\phi \rangle_\text{rms}\) (normalized by the free-fall (ff) velocity \(u_{ff} = \sqrt{agH}\)) as a function of height \(z\) for fixed \(r = 0.95R\) and of radius \(r\) at fixed \(z = H/2\). The height dependence of \(\langle u_\phi \rangle_\text{rms}\), Fig. 3(a), shows an anticyclonic (negative) circulation close to the top and bottom plates and an increasingly cyclonic (positive) circulation with increasing (decreasing) \(z\) from the bottom (top) plate. The radial dependence, Fig. 3(b), demonstrates the sharp localization of cyclonic motion near the sidewall as parameterized by the zero-crossing \(r_0\) (solid line) and the maximum \(r_{\text{rms}}\) (dashed line). Corresponding distances from the sidewall are \(\delta_\phi = R - r_0\) and \(\delta_{\text{rms}} = R - r_{\text{rms}}\)

\[\delta_{\text{rms}} \approx \delta_{\text{rms}}\] (based on maximum of rms of \(u_z\)). \(\delta_{\text{rms}}\) was used to define the sidewall Stewartson layer thickness in rotating convection [24], and our results for \(\langle u_\phi \rangle_\text{rms}\) are consistent with that description. What was absolutely not expected is the strong azimuthal variation of the instantaneous temperature \(T\) shown in Fig. 3(c), a feature that defines the global flow circulation, namely, the spatial distribution of the heat transport which is the origin of the bimodal temperature distributions seen in the experiments and DNS.

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mode-1 ($m = 1$) anticyclonic circulation in $\phi$ with a warm upflow on one side of the cell balanced by a cool downflow on the other side of the cell (for $\Gamma = 1, 2$, the dimensionless wave number $m/\Gamma = 2$ is independent of $\Gamma$, to be presented elsewhere). The anticyclonic circulation is the speed of the anticyclonic horizontal BL, suggesting that the thermal wave is anchored at the horizontal BLs so that it travels against the cyclonic circulation near the sidewall. The coherence between $T$ and $u_z$ leads to localization of vertical heat flux near the sidewall shown in Fig. 4(b). The unimodal PDFs are well fit by the sum of two Gaussians) from the DNS for $Ra = 10^9$, $1/Ro = 10$ in Fig. 5(b). The unimodal distribution for small $r/R$ bifurcates sharply to a bimodal distribution for $r/R \approx 0.72$. The corresponding experimental measurements do not provide data at intermediate $r/R$, but are consistent (dashed curve) with a scaled BZF width based on the scaling $Ra^{1/4}Ek^{2/3}$. Finally, the transition value of $1/Ro \approx 2$ from unimodal to bimodal distributions is roughly independent of $Ra$ as indicated in Fig. 5(c).

Our observations provide insight into experimental results for $\Gamma = 1/2$ in water with $Pr = 4.38$ [20, where the mode-1 LSC for nonrotating convection was reported to

FIG. 4. For $Ra = 10^9$ and $1/Ro = 10$: (a), (b) angle-time plots at $r = r_a, z = H/2$ of (a) $T$ and (b) $u_z$; (c) normalized time-averaged vertical heat flux $\langle F_z \rangle_h$ at $z = H/2$. In (c), location of $r$ where $\langle F_z \rangle_h = Nu$ (dashed-dotted line) and locations $r = r_0$ of $\langle u_y \rangle_l = 0$ (solid line) and $r = r_a$ of the maximum of $\langle u_y \rangle_l$ (dashed line) are shown. Color scale from blue (min values) to pink (max values) ranges (a) between the top and bottom temperatures, (b) in $[-u_{z1}/2, u_{z1}/2]$, (c) from 0 to midplane magnitude of $\langle F_z \rangle_h$, which is $\approx 3.4 Nu$.

FIG. 5. (a) Scaling of BZF widths $\delta_0$, $\delta_{u_{z1}}$, $\delta_{u_{z2}}$, and $\delta_{F_{z1}}$ with $Ek$ (DNS for $Ra = 10^9$); (b) Fitted peak values of bimodal PDF distributions (normalized by $\sigma$, standard deviation of $T$) at $z/H = 1/2$ vs $r/R$; DNS ($Ra = 10^9$) and measurements ($Ra = 8 \times 10^{12}$), both for $1/Ro = 10$; (c) diagram of the bimodal and unimodal temperature distributions at $r = R$, according to our DNS ($Ra = 10^9$) and experiments (larger $Ra$) of rotating RBC for $Pr \approx 0.8$ and $\Gamma = 1/2$. Critical inverse Rossby number equals $1/Ro_c = 2 \pm 1$ (shown with a dashed line).
transition into a then unknown state. Our BZF is that unknown global mode. We conclude that the BZF exists over a broad range of parameters $1/2 \leq \Gamma \leq 2, 0.1 \leq Pr \leq 4.4,$ and $10^8 \leq Ra \leq 10^{15}$ (details to be published elsewhere). Here, we presented details for $Pr = 0.8$ and $\Gamma = 1/2$ and for $Ra$ spanning 7 orders of magnitude [27]. A fully quantitative understanding remains a challenge for the future.

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[43] See Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevLett.124.084505 for evolution of the vorticity and temperature fields of the BZF.

Correction: The license statement contained an omission and has been fixed.