THE DOUBLE-DEGENERATE NUCLEUS OF THE PLANETARY NEBULA TS 01: A CLOSE BINARY EVOLUTION SHOWCASE

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ABSTRACT

We present a detailed investigation of SBS 1150+599A, a close binary star hosted by the planetary nebula PN G135.9+55.9 (TS 01). The nebula, located in the Galactic halo, is the most oxygen-poor known to date and is the only one known to harbor a double degenerate core. We present XMM-Newton observations of this object, which allowed the detection of the previously invisible component of the binary core, whose existence was inferred so far only from radial velocity (RV) and photometric variations. The parameters of the binary system were deduced from a wealth of information via three independent routes using the spectral energy distribution (from the infrared to X-rays), the light and RV curves, and a detailed model atmosphere fitting of the stellar absorption features of the optical/UV component. We find that the cool component must have a mass of $0.54 \pm 0.2 M_{\odot}$, an average effective temperature, $T_{\text{eff}}$, of $58,000 \pm 3000$ K, a mean radius of $0.43 \pm 0.3 R_{\odot}$, a gravity, $g = 5.0 \pm 0.3$, and that it nearly fills its Roche lobe. Its surface elemental abundances are found to be: $12 + \log \text{He}/\text{H} = 10.95 \pm 0.04$ dex, $12 + \log \text{C}/\text{H} = 7.20 \pm 0.3$ dex, $12 + \log \text{N}/\text{H} < 6.92$, and $12 + \log \text{O}/\text{H} < 6.80$, in overall agreement with the chemical composition of the planetary nebula. The hot component has $T_{\text{eff}} = 160–180$ K, a luminosity of about $\sim 10^4 L_{\odot}$ and a radius slightly larger than that of a white dwarf. It is probably bloated and heated as a result of intense accretion and nuclear burning on its surface in the past. The total mass of the binary system is very close to the Chandrasekhar limit. This makes TS 01 one of the best Type Ia supernova progenitor candidates. We propose two possible scenarios for the evolution of the system up to its present stage.

Key words: binaries: close – planetary nebulae: individual (PN G135.9+55.9, TS 01) – stars: AGB and post-AGB – stars: atmospheres – stars: evolution – stars: individual (SBS1150+599A)

Online-only material: color figures

1. INTRODUCTION

SBS 1150+599A was identified as a planetary nebula (PN) in Tovmassian et al. (2001) and subsequently designated as PN G135.9+55.9. More recently, we refer to this object as TS 01 (Stasińska et al. 2010). The object has unusually few spectral lines for a PN and is renown for its extremely low oxygen content (Tovmassian et al. 2001; Jacoby et al. 2002; Péquignot & Tsamis 2005; Stasińska et al. 2005, 2010). It is located above the Galactic plane at a distance of at least a dozen kpc, which places it among a handful of known halo PNe. Direct images obtained on the ground (Richer et al. 2002; Jacoby et al. 2002), and most recently by the Hubble Space Telescope (HST; Napiwotzki et al. 2005; Stasińska et al. 2010) confirm its PN identification. The observed expansion velocity of the nebula (Richer et al. 2003) is typical of PNe. But another outstanding feature of this PN is that it harbors a close binary system (Tovmassian et al. 2004), revealed serendipitously by the displacement of stellar lines with respect to nebular lines within a single observing night. Since only one component of the binary could be observed in the optical and UV, it was suggested that the visible component has a temperature of $110,000–120,000$ K. The lower limit is the minimum effective temperature needed to produce the observed [Ne v] nebular emission line, while the upper limit was deduced from the slope of the continuum (Tovmassian et al. 2004). There was an ambiguity in the determination of the orbital period, although it was clear that the nucleus is a close binary with a period less than 4 hr. The high temperature, coupled with high $log g$, determined from the profiles of absorption lines, led all studies prior to Stasińska et al. (2010) to assume that the observed optical/UV component was the central star of the PN, i.e., the post asymptotic giant branch (AGB) star that lost its envelope and was the source of its ionization. Péquignot & Tsamis (2005) suggested that, if the ionizing star were even hotter, the deduced oxygen abundance could be increased to a more common level for oxygen-poor PNe. However, a higher temperature would have required a higher reddening to match the observed continuum slope, and Tovmassian et al. (2004) had already used a higher extinction than would normally be estimated for the direction of SBS 1150+599A in order to justify a temperature of 120,000 K.

Next, we obtained photometric light curves of the binary core of SBS 1150+599A (Napiwotzki et al. 2005). The orbital period of the system turned out to be 3.92 hr and, to explain the double-humped shape of the light curve, we were led to invoke a Roche lobe-filling optical/UV component. It was observed

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that the depths of the minima in the light curve are uneven, an effect known to occur when the visible component is irradiated by a hotter (more energetic) source. The orbital dynamics required that this invisible component be another compact object of at least 0.85 $M_\odot$ (Napiwotzki et al. 2005). Jacoby et al. (2002) pointed out the possibility that SBS 1150+599A may be associated with the X-ray source 1RXS J115327.2+593959.

To detect the invisible source of irradiation and reveal the other component of the close binary, we observed it with the XMM-Newton X-ray observatory. We also conducted new optical spectroscopic observations of the object with the Gemini-North telescope to improve our knowledge of RVs of the optical/UV component of the binary and to better fit photospheric line profiles with atmospheric models. We also used the publicly available HST Space Telescope Imaging Spectrograph (STIS) observations of the object in the UV to bridge the optical and X-ray observations discussed here.

The ionization state and chemical composition of the PN are analyzed in a companion paper (Stasieńska et al. 2010), while here we present a multifaceted analysis and modeling of the binary system. We analyze the history and the future of the stellar system in the light of evolutionary models for close binary stars.

In Section 2, we present our new observations; in Section 3, we determine the physical parameters of the binary; in Section 4, we discuss the evolution of the object from the early stages, when it was a wide system comprised of main-sequence (MS) stars, to the latest stage of a merging of two white dwarfs (WDs) with possible Type Ia supernova (SN Ia) outcome; and in Section 5 we summarize our main results.

2. OBSERVATIONS

2.1. Optical Observations

A spectrum of TS 01, with an ample coverage of 3800–9200 Å is available in the Sloan Digital Sky Survey (SDSS10). It was taken on 2002 May 17 (spSpec-52411-0953-160). We used the newly calibrated spectrum that appears in the SDSS Data Release 7. This spectrum provides probably the best flux calibration, in a perfect agreement with HST spectra (see below).

The stellar absorption lines of the Balmer series and of He II are difficult to detect due to their shallowness, the faintness of the object (V ~ 18m), and the presence of very intense emission lines from the nebula. Only seven spectra with measurable absorption features were available from our Canada–France–Hawaii Telescope (CFHT) observations (Tovmassian et al. 2004). The short orbital period and consequent line smearing by the long exposures, and the necessity of relatively high resolution to effectively disentangle emission lines from absorption indicated the need for observations with a larger telescope.

We proposed to observe TS 01 for a total of 16 hr, covering four orbital periods, with Gemini-North telescope. The observations were scheduled for service mode in semester 2006A, but only 20% were completed. The available observations were performed in two sets: on 2006 May 16 UT, eight spectra were obtained, and, on 2006 June 9, four more were added. The weather conditions during the observations were not ideal. The exposure times were 700 s, so, in total, only about 3/4 of the orbital period was covered with a resolution in phase of 5%. The GMOS spectrograph was used with the B1200+G5301 grating, leading to an effective spectral resolution of 1.65 Å (FWHM) and a spectral coverage of 3800–5000 Å. We observed the Balmer series from H$_\beta$ to the highest members (H$_\beta$). This spectral range also includes the He II 4686 Å line, detectable in both emission and absorption. Auxiliary images (biases, flat fields, arcs) were used to reduce the data using the procedures in gemini package within IRAF11 and prescriptions provided by Gemini staff and fellow observers.12 The standard star PG 1545+035, observed with the same instrumental configuration on 2006 August 30 in apparently better conditions, was used in an attempt at flux calibration. However, the result of this calibration was not satisfactory. Instead, we used the spectrum of TS 01 available in the SDSS database to correct the continuum. The Gemini spectra were corrected for orbital radial velocity (RV) shifts using the orbital solution described below and then co-added. Combining the 12 RV-shifted spectra allowed us to improve the profiles of stellar absorption lines and to get rid of nebular emission lines. The resulting spectrum, after 13 pixel boxcar smoothing, is presented in Figure 1.

Previous observations of TS 01 are used here to analyze the nature of the stellar core. In addition to the above mentioned seven CFHT spectra of lower spectral resolution, they include multiband photometric observations, briefly presented in Napiwotzki et al. (2005). They were obtained on two consecutive nights with the 2.2 m telescope at Calar Alto and the BUSCA CCD camera system that allows simultaneous direct imaging in four colors. The differential photometry was performed using comparison stars in the field of view. These photometric data were complemented by CCD photometry in the V filter obtained with the 2.1 m telescope at the Observatorio Astronómico Nacional in the Sierra de San Pedro Mártir (OAN SPM) on 2004

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10 http://www.sdss.org

11 Copyright(c) 1986 Association of Universities for Research in Astronomy Inc.

12 http://www.astro.caltech.edu/~kelle/gmos/gemini_reduction.html

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Figure 1. Stellar spectrum of TS 01 obtained at Gemini-North (solid red line). The spectrum is a combination of 12 individual spectra, observed at different orbital phases, and smoothed with a 13 pixel boxcar. Before combining, the individual spectra were corrected for orbital motion. The SDSS spectrum, containing nebular lines, is plotted in yellow. The black dotted line is the single HST spectrum obtained for the same spectral range (see the text). (A color version of this figure is available in the online journal.)
April 9. Additional photometric data were provided by the optical monitoring (OM) instrument on board XMM-Newton during the X-ray observations. Optical and UV data from direct images in the optical range as well as integrated flux from spectroscopic observations were also incorporated into the time series. For the time series analysis, the photometric data from the different wavelengths and bandpasses were normalized to a common mean value and combined.

2.2. Ultraviolet Observations

The first UV data for TS 01 were obtained in the far-UV using the Far Ultraviolet Spectroscopic Explorer (FUSE) satellite. Details of these observations and their results are provided in Tovmassian et al. (2004).

Later, observations in the near-UV were obtained with the HST (Obs. ID 9466). In 2003 May, HST obtained spectra of TS 01 with the STIS in FUV, NUV, and CCD modes to cover the entire UV and optical. Continuous (uninterrupted by the Earth occultations) exposures with the G140L and G230L gratings were acquired. Five spectra with each grating and with individual exposure times of 4675 s and 2850 s, respectively, were acquired and combined to produce the final spectrum. One 600 s exposure was taken of the UV-optical spectrum (G430L grating) to connect the UV data with the optical. This last spectrum, as a result of its short exposure time, fails to reveal relatively weak, though important, emission lines in the optical spectrum, as a result of its short exposure time, fails to reveal relatively weak, though important, emission lines in the optical spectrum, but provides a decent stellar spectrum that overlaps nicely with the NUV and SDSS spectra. This spectrum is also plotted UV, but provides a decent stellar spectrum that overlaps nicely with the NUV and SDSS spectra. This spectrum is also plotted in Figure 1 and is in very good agreement regarding absorption features. The object was also observed in 2003 June with High Resolution Camera (HRC) of the Advanced Camera for Surveys (ACS) in the F334N & F658N filters to obtain images in the strong nebular lines of [Ne v] and Hα, respectively.

The pipeline-reduced STIS spectra were utilized to extract the stellar continuum. The integrated fluxes of individual exposures in UV range were also summed to produce a light curve in the UV range.

2.3. X-ray Observations

TS 01 was observed with XMM-Newton (Obs. ID 0404220101) on 2006 November 1–2 (revolution 1263) in a continuous 27 ks exposure. The X-ray-counting EPIC instruments were operated with the thin filter in the PN small window mode and full window for the MOS detectors. The object was too faint for EPIC-RGS detectors. The OM instrument on board XMM-Newton took 16 images in a B filter, each of 22 minutes duration. No pile-up was detected in either of the EPIC detectors. Background photon flares were detected during only 35%–40% of exposure, mostly toward its end. The 7.5 hr exposure is just shy of two orbital periods (2 × 3.9 hr) of the binary system. The data from the first orbit were completely free from background flaring effects. The observed mean source count rates were 0.033 ± 0.002 in the PN, 0.0025 ± 0.0004 and 0.0053 ± 0.0005 counts s⁻¹, in the MOS1 and MOS2, respectively.

The data were reduced using XMM-SAS (version 9.0). For the MOS detector, the source and background photons were extracted from a circular aperture and surrounding annulus correspondingly. For the PN detector, we tried subtraction of background from two different circles near the source, since the small window did not allow one to use a large annulus. We found no substantial differences in background removal from different areas. Events with detection patterns of up to quadruples were selected.

Background-subtracted spectra in the three EPIC detectors and a single blackbody model corresponding to each detector are shown in Figure 2. Estimates of the total galactic H I column density varies from N_H = 1.8 × 10²⁰ (Kalberla et al. 2005) to N_H = 1.53 × 10²⁰ cm⁻² (Dickey & Lockman 1990). The X-ray spectral analysis, with the column density fixed to the mean value determined for the direction of TS 01 (N_H = 1.6 × 10²⁰ cm⁻²), gives a best fit for kT = 17 eV (T ≈ 195,000 K). Based upon the XSPEC (Arnaud 1996) modeling, the 90% confidence region spans kT = 12.7–18.0 eV. The source is extremely soft and emits only in the narrow range spanning 100–300 eV. This range is notorious for its unreliable calibration (e.g., Mateos et al. (2009) for the latest evaluation) and routinely excluded by observers. However there is a good agreement between flux in the PN and MOS detectors for 0.1–0.3 keV (Figure 2). Although the PN detector suggests the possibility that there is emission in excess of the blackbody in the 0.4–0.5 keV bin, the excess is not confirmed by either of the MOS detectors, making it unlikely that it is a real spectral feature. The analysis of ROSAT RASS archival data reveals that the source was poorly covered and the background is uneven, making spectral fitting useless, though it does confirm the extreme softness of the source.

In Figure 3, the light curve of the source in the PN detector is presented extracted in two energy bands, 0.1–0.3 keV and 0.3–10 keV. This light curve demonstrates that practically all photons from the source are emitted in the narrow soft band, that the background flaring occurs mostly in the last quarter of the 27 ks exposure, and that the flares do not affect the soft band, while the source emits, but are rather strong in higher energies, confirming their nature as background. A similar picture emerges from the MOS detectors. However, we have chosen a conservative approach and excluded all episodes when the count rate exceeded 0.1 counts s⁻¹ from the analysis of the source in all three detectors.

The X-ray light curve of the source in the PN detector shows some flickering but no definite periodic variability. There is no
The orbital parameters were roughly determined with the discovery of the binarity (Tovmassian et al. 2004). However, band photometry from HST data were used to identify the precise orbital phasing for the X-ray ground-based optical differential photometry. In this way, they taking the logarithm and shifted to the same average value as the reduction were simply transformed into a magnitude scale by considering the integrated flux in narrow bands from UV spectra of a period using the discrete Fourier transform (DFT) method.

The possible interpretation of the double humped light curve was briefly discussed in Napierwotzki et al. (2005). With the X-ray observations in hand we are now confident that the double hump is a result of the surface projection of the ellipsoidal binary component that fills its Roche lobe and orbits its more massive companion on a relatively high-inclination orbital plane (to the line of sight), coupled with the effect of gravitational darkening. The difference in minima dips, on the other hand, is the consequence of the heating of the surface of the Roche lobe-filling component, since it is the main contributor of light to the hotter component which irradiates its cooler companion. We refrain from the usual wording of primary and secondary components in this paper, since, as we later discuss, the roles of primary and secondary changed during the evolution of this system.

The optical spectra are too sparse to determine the orbital period independently, but they cover almost all orbital phases. The resulting ephemeris is

\[ \text{HJD} = 2452760.6756(5) + 0.1635083(3) \times E, \]

where the zero point \( T_0 \) corresponds to the deeper minimum in the light curve. The light curves of TS 01 folded with the estimated 3.924 hr orbital period are presented in Figure 5 in different bands. In the bottom panel, multi-color photometry from Calar Alto is plotted combined with \( V \) band data from OAN SPM and OM-XMM. In the top panel, the measurements from a variety of HST detectors are displayed. Even though the \( HST \) data in the optical narrow filters F334N & F658N include large contributions from the nebular emission lines, they nevertheless show variability of the stellar core with a similar amplitude as in the broadband filters. The UV light curves have the same double-humped shape as their optical counterparts, but the amplitude decreases as the wavelength moves further into UV. The far UV observations with the G140L grating have exposures that are almost a quarter of the orbital period, so orbital smearing is severe. Degrading the optical light curves to a similar time resolution shows that the small amplitude in the far UV light curve is the result of smearing rather than an actual change in the amplitude of the variation.

The optical spectra are too sparse to determine the orbital period independently, but they cover almost all orbital phases. The

![Figure 3. X-ray light curve of the source in the PN detector (top panel). The filled symbols represent the light curve in the 0.1–0.3 keV range, while the open symbols (yellow) are the counts in the 0.3–10.0 keV band. The count rate above 0.3 keV is practically zero, except during the final part of the exposure, where they are dominated by background flaring. In the extreme soft band, 0.1–0.3 keV, the count rate is approximately constant (0.033 counts s\(^{-1}\)) for the entire duration of the observation. The bottom panel displays the optical light curve for comparison. Black points are OM measurements on board of XMM-Newton at the time of the observations whereas the open boxes are \( V \) light curve obtained at SPM (2.5 yr earlier; shifted in time according to phases). (A color version of this figure is available in the online journal.)

![Figure 4. Power spectrum of all photometric data. The strongest, single peaked maximum corresponds to the orbital period, at 6.1159 day\(^{-1}\). The first harmonic, at \( \approx 12 \) days\(^{-1}\), is also prominent in the power spectrum because of the double-humped nature of the light curve.](image)
The upper panel presents Tovmassian et al. (2004) adding the new parameter determination procedure (Napiwotzki et al. 2004). We are able to construct the RV curve. We used the FITSB2 measuring the RVs of the absorption features in each spectrum, to calculate the orbital phases for the spectra. Therefore, by introducing best guesses for the temperature composition of the binary (Tovmassian et al. 2007), the best fits were achieved with $T_{\text{eff}} = 60,000 \pm 5000$ K, log $g = 5.17 \pm 0.07$.

The RV curve presented in Figure 6 is fitted with a simple sinusoid. The phase zero corresponding to the $-/+\pi$ crossing of the RV curve coincides with the deeper minimum in the light curve. It confirms our interpretation that, at phase 0.0, the optical component is seen in conjunction from behind, turning to the observer its smallest projected area and coolest surface temperature. At phase 0.5, the optical component is seen with the same projected area, but presents the face with the highest temperature, as result of the intense heating from the X component. A formal orbital solution leads to semi-amplitude of RV $K_{\text{cool}} = 216 \pm 10$ km s$^{-1}$, and systematic velocity of the system $\gamma = 0 \pm 12$ km s$^{-1}$ relative to the nebular emission lines.

The correct determination of phases and RVs allowed us to combine all 12 Gemini spectra, eliminating the nebular emission line components, and delineating the absorption profiles with increased signal to noise. The co-added spectrum is shown in Figure 1. In combination with the UV stellar spectra from the HST observations, where the stellar component is easily separated from the nebular one due to the high spatial resolution, the co-added spectrum allows us to perform a model atmosphere analysis of the cool component (see Section 3.2).

### 3.2. Temperatures and Radii

TS 01 is clearly the first PN known to contain a double-degenerate binary (De Marco et al. 2008). The first indication that the previous interpretations (Tovmassian et al. 2004; Péquignot & Tsamis 2005) of the central star of TS 01 may be incorrect came from the shape of its light curve (Napiwotzki et al. 2005). Now, armed with the X-ray data, we know that even a 130 K K star cannot produce the observed X-ray flux and that an additional component is required to explain the observed spectral energy distribution (SED).

We analyze the SED, fitting it with a blackbody as a first approximation. The actual atmosphere can be significantly different from a blackbody at wavelengths shorter than 900 Å, but as a starting point a blackbody gives us a good idea of what we are dealing with. We will discuss deviations from blackbody later in the paper. The data were de-redden according to Schlegel et al. (1998) with a canonical ratio of total-to-selective absorption, $E(B-V) = 0.03$ mag and $R_V = 3.1$.

We simultaneously fit two blackbodies to the observed SED by introducing best guesses for $T_{\text{cool}}$, $T_{\text{hot}}$, $r_{\text{cool}}/D$, and $r_{\text{hot}}/D$, where $D$ is the distance to the object, and calculating their best-fit values. Since there is a gap between extreme UV and X-ray wavelength ranges, and since the slope of the X-ray data is not strictly that of a blackbody, we obtain three distinct solutions with similar $\chi^2$ by varying the input parameters. Possible solutions are presented in Table 1.

The resulting fits are presented in Figure 7. The blackbody solution for the hot component is $T_{\text{hot}} \approx 180,000 \pm 25,000$ K. Minimum $\chi^2 \approx 2.6$ can be achieved with significantly different temperatures for the hot component, depending upon which part of X-ray data the fit relies on. But the hot solutions with
Thus, only a cool component flux does not provide enough irradiation to the hot component between the maxima of the light curve. To restrict the range of possible solutions, we analyze the form of the required difference in the depths of minima of the light curve. In this area the luminosity of the cool component determined from the light curve analysis starts to deviate from that value, we find that regardless of other poorly constrained parameters of the cool component in Nightfall to that value, we find that regardless of other poorly constrained parameters of the cool component in Nightfall, the mass limit is actually 0.54 $M_\odot$. Fixing the mass of the cool star in Nightfall to that value, we find that regardless of other poorly constrained parameters of the cool component, the cool star must have a radius of at least 0.42 $R_\odot$ to fill its Roche lobe up to 94%–99% in order to produce the observed light curve. Since the cool component is ellipsoidal in shape, this radius, as determined by Nightfall, represents the mean radius. In fact, the radius depends only weakly on the mass adopted for the star, and is a stronger function of the binary system’s mass ratio, which determines the size of Roche lobe. For range of mass ratios stemming from the total mass of the system in 1.3–1.45 $M_\odot$ interval the mean radius of the cool component lies within the 0.42–0.45 $R_\odot$ range.

The mass and radius obtained for the cool component leads to a mean log $g$ of 5.03 ± 0.03, a value deduced by averaging the unevenly distributed gravitational acceleration on its surface.

### Table 1

| Solution | Optical Component | X Component |
|----------|-------------------|-------------|
|          | $T$ (K) | $R/D$ ($\times 10^{-13}$) | $D^\circ$ | $T$ (K) | $R/D$ ($\times 10^{-13}$) | $R^\circ$ | $\log L^\circ$ | $\chi^2$ |
| Cool     | 47,700 | 3.80 | 21.7 | 152,600 | 1.20 | 0.12 | 3.81 | 2.54 |
| Intermediate | 58,900 | 3.83 | 21.6 | 174,600 | 0.43 | 0.04 | 3.14 | 2.63 |
| Hot      | 60,600 | 3.83 | 21.5 | 205,200 | 0.15 | 0.014 | 2.51 | 2.65 |

Note. The values of these columns were calculated assuming $R_{\text{cool}} = 0.43 R_\odot$, and corrected by a factor $D \sim \sqrt{T} = 0.85$ because the model atmosphere flux $F_{\text{atm}} \approx 0.73 \times F_{\text{BB}}$ with $T = T_{\text{eff}}$ at the optical wavelengths, as it follows from the analysis below (see Sections 3.2.1 and 3.2.2).

Figure 7. SED of TS 01. The observed spectra are presented by crosses with error bars (SDSS + HST/STIS + FUSE+XMM). The observations are fitted with two blackbodies. Three pairs of blackbody solutions are presented according to Table 1. Dashed, dash-dotted and dotted lines represent the cool, the hot components, and their sum, respectively. Shaded is the area in which the radius of hot component determined from the light curve analysis starts to deviate from the one required for SED fitting. In this area the luminosity of hot component does not provide enough irradiation to the cool component to produce observed light curve. Thus, only a cool $\sim160,000$ K solution is viable.

$T_{\text{hot}} \gtrsim 175,000$ K, marked in the Figure 7 as shaded area, do not work, as can be seen below, because only certain ratios between the hot and cool components fluxes can produce the required difference in the depths of minima of the light curve. To restrict the range of possible solutions, we analyze the form of the light curve, together with the RV curve, using the binary star modeling code Nightfall.13

Nightfall is based on a physical model that takes into account the non-spherical shape of stars in close binary systems, as well as the mutual irradiation of both stars, and a number of additional physical effects such as gravitational darkening and albedo. We fitted simultaneously the light curves in three bands and the RV curve. The program uses differential magnitudes and is tailored to the Johnson photometric system. Taking into account that the shape and range of amplitudes of the light curve is (1) similar in the BUSCA narrow filters and the Johnson V filter and (2) does not show large wavelength dependence in the optical range, we assigned BUSCA $uv$ to the $U$ filter, $b$ to the $B$ filter, and $r$ to the $R$ filter. We did not use nir band data, since it was the noisiest and would not add anything substantial to the analysis.

We searched for solutions by setting the temperatures to the values estimated from the SED. We also fixed the total mass of the system close to the Chandrasekhar limit of 1.39 $M_\odot$. The real $M_{\text{nuc}}$ might be slightly lower or higher, that would not affect this analysis. Leaving the total mass parameter free, Nightfall tends to solutions involving massive stars, which are excluded. However, limiting the total mass still results in a variety of remaining parameters that achieve similarly good fits.

To restrict the possible solutions, we analyze the form of the light curve, together with the RV curve, using the binary star modeling code Nightfall.

3.2.1. The Cool Component

The first estimate of the mass of cool component (Tovmassian et al. 2008, 2007) based on $T_{\text{eff}}$ and evolutionary tracks for solar composition post-AGB stars from (Schoenberner 1983; Bloeker 1995) led to $M_{\text{cool}} \approx 0.58 M_\odot$. Recent models for different metallicities (Weiss & Ferguson 2009) suggest $0.52 M_\odot$ as the lower limit of the mass of a star that heats up to $\sim 60,000$ K (see Figure 8). For $Z = 0.001$, the mass limit is actually 0.54 $M_\odot$. Fixing the mass of the cool component in Nightfall to that value, we find that regardless of other poorly constrained parameters of the cool component, the cool star must have a radius of at least 0.42 $R_\odot$ to fill its Roche lobe up to 94%–99% in order to produce the observed light curve. Since the cool component is ellipsoidal in shape, this radius, as determined by Nightfall, represents the mean radius. In fact, the radius depends only weakly on the mass adopted for the star, and is a stronger function of the binary system’s mass ratio, which determines the size of Roche lobe. For range of mass ratios stemming from the total mass of the system in 1.3–1.45 $M_\odot$ interval the mean radius of the cool component lies within the 0.42–0.45 $R_\odot$ range.

The mass and radius obtained for the cool component leads to a mean log $g$ of 5.03 ± 0.03, a value deduced by averaging the unevenly distributed gravitational acceleration on its surface.

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13 [http://www.hs.uni-hamburg.de/DE/Ins/Per/Wichmann/Nightfall.html](http://www.hs.uni-hamburg.de/DE/Ins/Per/Wichmann/Nightfall.html)
absorption line ratio. We find $T_{\text{NUV}}$ observations and with the Figures 9(a) and (b), comparing a TMAP model with the STIS a good agreement with the observed spectral line profiles (see $Z$ 2009 and A. Weiss & J. W. Ferguson 2009, private communication). Solid line: $Z$.

(Djurasevic 1992). A very similar value of surface gravity is obtained by using FITSB2 (Section 3.1).

Next, we modeled the stellar atmosphere of the cool component using the Tubingen NLTE Model-Atmosphere Package (TMAP) (Werner et al. 2003; Rauch & Deetjen 2003). This code computes plane-parallel or spherical non-LTE model atmospheres in radiative and hydrostatic equilibrium and considers opacities of all species from hydrogen to nickel. The determination of $T_{\text{cool}}$ is based on the evaluation of the ionization equilibrium through the C iv 1175 Å/C iv 1169 Å stellar absorption line ratio. We find $T_{\text{cool}} = 55 \pm 5$ kK. At such a temperature, a surface gravity of $\log g_{\text{cool}} = 4.9 \pm 0.5$ gives a good agreement with the observed spectral line profiles (see Figures 9(a) and (b), comparing a TMAP model with the STIS NUV observations and with the gemini spectrum, respectively). $T_{\text{cool}}$ and $g_{\text{cool}}$ cannot be better constrained given the quality of the data. However, the agreement between the values derived with TMAP and those derived with FITSB2 and Nightfall confirms our correct assessment of the basic parameters of the cool component.

We performed some TMAP test calculations in order to derive upper abundance limits for some metals. These are summarized in Table 2. Note that the resonance lines of C iv and N v were not used in our abundance determination, since they were found to be affected by interstellar line absorption. The chemical composition of the cool stellar component is close to that of the nebula (Stasińska et al. 2010).

In Figure 10, the model is compared with observations, covering continuously the whole range from 900 to 10000 Å. Apart from the observations and atmospheric model, the nebular emission is shown as deduced in Stasińska et al. (2010), and the blackbody curves as implemented in Nightfall. The blackbodies corresponding to the cool and hot components are denoted by open stars (red and blue, respectively). The sum of the two blackbodies and the nebular continuum within the observing slit as computed in Stasińska et al. (2010) is represented with the thick red line in Figure 10. The fit of the models to the observations is excellent from the near infrared to 1500 Å.

The curve representing the stellar model plus the nebular emission departs slightly from the observations at shorter wavelengths. The problem with the flux above 1500 Å in the NLTE models has been noted before (Rauch 2008). More importantly, the model is calculated for a spherically symmetric star with a homogeneous temperature distribution over its surface. However, we know that the cool component is strongly irradiated and gravitationally distorted, which affect both its SED.

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**Table 2**

| Element          | Mass Fraction |
|------------------|---------------|
| H                | 7.471E-01     |
| He               | 2.525E-01     |
| C                | 1.335E-04     |
| N                | <8.306E-05    |
| O                | <7.116E-05    |
| Si               | <6.737E-05    |
| Ca–Ni            | <1.319E-06    |

**Notes.** Ca–Ni are represented by a generic model atom. The errors for H, He, and C are about 0.3 dex. For N, O, Si, and the iron-group elements upper limits are given.

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http://astro.uni-tuebingen.de/~rauch/TMAP/TMAP.html

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Figure 8. $T_{\text{eff}}–\log g$ dependence for post-AGB models (Weiss & Ferguson 2009 and A. Weiss & J. W. Ferguson 2009, private communication). Solid line: $Z = 0.004$ for 0.529 and 0.533 $M_\odot$. Dashed line: $Z = 0.0005$ for 0.539 and 0.551 $M_\odot$, correspondingly. Tracks for more massive stars spread out toward hotter temperatures. The ellipse indicates the range of possible solutions for TMAP and those derived with FITSB2 and Nightfall.

Figure 9. Comparison of a TMAP SED with observation. (a) the STIS NUV range. The He ii Fowler series (marked at top) are well reproduced; “is” denotes interstellar lines. (b) the Gemini-North optical range. The H and He lines are marked at top.

(A color version of this figure is available in the online journal.)
and the gravitational acceleration over the surface of the star. We approximate the observed, phase-averaged spectrum by the non-irradiated atmosphere model even though, in some orbital phases, we observe the irradiated hemisphere of the cool component. The spectra of irradiated atmospheres are flatter in the optical range than those of non-irradiated atmospheres. The thick black line is the sum of the model continuum emission from the nebular and stellar components. The blackbody solutions are presented by red open stars for the cool component and by blue stars for the hot component. The thick red line is sum of hot (162 kK) and cool (∼57 kK) blackbodies plus nebular emission.

3.2.2. The Hot Component

The parameters of the hot component are less certain. Our knowledge of the hot component is based on the binary period, the fact that the cool component is partially irradiated to produce the observed light curve, and the X-ray flux, which cannot originate from the cool component. There is an extensive argument in Napiwotzki et al. (2005) discussing why the hot component should be a compact object with a mass exceeding the mass of the cool component. However, neither the light curve, nor the X-ray spectra allow us to determine the temperature or radius of the hot component as well as we did for the cool component.

We face two problems in the case of TS 01’s hot component. First, TS 01 is only detected in short, soft end of the X-ray range. Second, the calibration of data at the extreme soft end of the XMM-Newton spectral range is not very reliable. Both prevent us from fitting exact atmospheric models to it. Hence, like most studies of SSS, we are forced to continue the analysis using the blackbody that successfully describes the spectrum of the hot component in the optical and UV range up to $4 \times 10^{15}$ Hz (see Figure 7). We also note that this introduces an overestimate of the luminosity of the X-ray source (Heise et al. 1994; Swartz et al. 2002). On the other hand, the temperature can be either overestimated (Swartz et al. 2002), or underestimated (Heise et al. 1994; Ibragimov et al. 2003). Therefore, when estimating the temperature of the hot component in the optical/UV range separately from estimates in X-rays, we should not worry too much if discrepancies arise. It is within the optical/UV range that the irradiation of the cool component matters, so we may fix the parameters of the cool component in Nightfall and seek solutions for the hot component. Even so, varying freely both the radius and temperature of hot component, we still do not reach unambiguous solutions.

In Figure 11, we present the fits produced by Nightfall to light curves in three different filters. The parameters for the fits for the different temperatures of the hot component are presented in Table 3. The temperature and the mass of the cool component were kept fixed (the difference in mean temperatures of the cool component in the table reflects the different degree of irradiation). The parameters that were fitted are the orbital inclination angle, the fraction to which both components fill their Roche lobes, and the temperature of the hot component. Three models with different temperatures for the hot component are displayed in Figure 11. The fits shown red, green, and blue correspond to $T_{\text{hot}} = 162, 182,$ and 202 kK, respectively. The lower and upper panels show the deviations of the fit from the observations for the extreme cold and hot solutions. As can be seen from Figure 11 and Table 3 the differences between three models ranging from 160 to 200 kK are not important in the optical domain.

Note that the range of temperatures for hot components obtained from blackbody fitting to SED and from the fitting of light curves by Nightfall is similar. But comparison of Tables 1 and 3 shows that only for low temperature solution the radii deduced by both methods are compatible. Introducing the radius of the cool component deduced from Nightfall into the $R_{\text{cool}}/D$ parameter used in the fit of two blackbodies to the SED results in a distance of 25 kpc for the minimum radius of $R_{\text{cool}} = 0.42 R_{\odot}$ and leads to $R_{\text{tot}} \approx 0.13 R_{\odot}$ for a blackbody temperature 150 kK. The color temperature of the hot component is probably slightly higher. This is caused by the divergence of the real atmosphere from the blackbody at high energies and also by the use of a Roche-lobe-shaped cool component in Nightfall, instead of the spherical shape in all other calculations. Similarly, using stellar atmospheres instead of blackbodies reduces the distance to about 21 kpc, as reflected in Table 1. Increasing temperature is compensated naturally by a smaller radius. The solutions with temperatures above 175 kK come up with parameter $R_{\text{rot}}/D$ too small to be compatible with results of light curve fitting. In Figure 7, the blackbody solutions of hot component that fall into shaded area are not luminous enough to provide necessary irradiation and produce the observed light curves. In the meantime, temperatures above 185 kK are not tolerated by ionization modeling of the nebula (Stasińska et al. 2010).

Therefore, we consider 160–175 kK temperature range and $R_{\text{rot}} \approx 0.1 R_{\odot}$ to be the closest to the real properties of the hot component. Note that the hot component has a radius $R_{\text{rot}} \geq 0.04 R_{\odot}$ at least. This is much larger than an ordinary WD. As such TS 01’s hot component is very similar to the supersoft X-ray source (SSS) Lin 358, one of the two SMC symbiotic stars studied by Orio et al. (2007). Majority of estimates of temperatures and luminosities of SSS are made using blackbodies and values obtained here are useful when comparing to other similar objects.
Fitting an exact atmospheric model to the X-ray data for the hot component does not make much sense, because the observed energy range is too small and the quality of the data is too poor.15

An additional test for checking the estimated temperature of the hot component comes from modeling of the light curve in the UV. However, Nightfall cannot calculate model fluxes in the UV, so we implemented our own code (Shimansky et al. 2002), which calculates the irradiation in a binary according to the prescription in Howarth & Wilson (1983). Nightfall is based on the same algorithm, so we naturally obtained exactly the same light curves for optical bands. We compute the UV light curves for the cool solution from Table 3, and present it, together with the observed one, in Figure 12. In computing the UV light curves we take into account the difference between a blackbody and a stellar atmosphere introducing the ratio \( f_\lambda = F_\lambda(BB)/F_\lambda(BSA) \) of blackbody and a stellar atmosphere fluxes at a given wavelength.16

### Table 3

| Solution | Opt/UV | Component | X | Component |
|----------|--------|-----------|---|-----------|
|          | \( T \) (K) | \( M \) (\( M_\odot \)) | \( R \) (\( R_\odot \)) | \( \log g \) | Inc (deg) | \( T \) (K) | \( M \) (\( M_\odot \)) | \( R \) (\( R_\odot \)) | \( \log g \) | \( \chi^2 \) |
| Cool     | 57 100 | 0.537     | 0.44 | 5.02 | 52.8 | 162 195 | 0.853 | 0.135 | 6.1 | 46.27 |
| Intermediate | 57 264 | 0.537     | 0.43 | 5.04 | 53.0 | 182 195 | 0.853 | 0.113 | 6.3 | 46.37 |
| Hot      | 57 104 | 0.537     | 0.43 | 5.04 | 53.2 | 202 000 | 0.853 | 0.088 | 6.5 | 46.43 |

3.3. The Total Mass

The mass of the hot component cannot be determined directly from the observed data. However, simultaneously fitting the RV curve and light curves indicates a tendency toward improvement as the total mass approaches the Chandrasekhar limit. In Figure 13, we plot the calculated \( \chi^2 \) as a function of the total mass of the system, by fixing in Nightfall the temperatures of the components to our best estimates, i.e., 57 and 162 kK and adopting a mass of 0.54 \( M_\odot \) for the cool component. The lower limit for total mass is of 1.25 \( M_\odot \), corresponding to a hot component with a mass of \( \sim 0.7 M_\odot \). This mass corresponds to the lower limit for a WD to sustain steady nuclear burning on its surface. Increasing the total mass of the binary from that minimum value produces a decrease in the \( \chi^2 \) value, with a small plateau of \( \chi^2 \) at about 1.4 \( M_\odot \). The \( \chi^2 \) keeps falling as the total mass increases. This is due to the fact that rising mass of the hot component shrinks the Roche lobe of the cool star. At around \( M_{\text{total}} = 1.47 \) the cool component fills its corresponding Roche lobe to 99.9%, which helps a better fitting of the light curves. Improvement of \( \chi^2 \) from there on is conditioned by the rapid increase of size (Roche lobe-filling factor \( = ff \)) of the hot component, which might be unrealistic. The mass could in principle be constrained by the fit to the RV curve, but unfortunately the RV data are too poor in quantity and quality to have strong influence on \( \chi^2 \). We consider the flattening of the \( \chi^2 - M_{\text{total}} \) curve around \( M_{\text{total}} = 1.40 \) as an indication of the best solution, where a balance is achieved between fitting the light and RV curves at the same time, but of course a lower than Chandrasekhar limit mass is not excluded. Better measurements of RVs are required for a more reliable determination of stellar masses in TS 01.

The mass estimate of the hot component can be checked from its position in the H–R diagram (Suleimanov & Ibragimov 2002), which calculates the irradiation in a binary according to the prescription in Howarth & Wilson (1983). Nightfall is based on the same algorithm, so we naturally obtained exactly the same light curves for optical bands. We compute the UV light curves for the cool solution from Table 3, and present it, together with the observed one, in Figure 12. In computing the UV light curves we take into account the difference between a blackbody and a stellar atmosphere introducing the ratio \( f_\lambda = F_\lambda(BB)/F_\lambda(BSA) \) of blackbody and a stellar atmosphere fluxes at a given wavelength.16

15 For the analysis of the ionization of the nebula, however, using a blackbody would cause serious problems at high energies. This is why, for their photoionization modeling, Statistlka et al. (2010) selected a suitable spectrum from a grid of models with halo composition, which reasonably well describes the observed fluxes both in opt/UV and X-ray range and provides a more realistic picture.

16 In the optical part of the spectrum \( f_{\text{opt}} \approx 0.73 \) for both the cool and hot components; near the Lyman edge theSED of the cool component is different from a blackbody: \( f_{\text{5350}} \approx 1.18 \) and \( f_{\text{1555}} \approx 1.02 \); the values of \( f_{\lambda} \) for the hot component remain close to 0.73. Moreover, the values of \( f_{\lambda} \) for the cool component must depend on the irradiation flux. If the irradiation flux increases, \( f_{\lambda} \) decreases, because the spectra of the irradiated stellar atmosphere are getting closer to a blackbody spectrum. The best approximation of the observed light curves by the model light curves was obtained for a simple linear dependence \( f_{\lambda} = a - b \cdot (F_{\text{irr}}/F_0) \), where \( F_{\text{irr}} \) is the irradiation flux at a given point of the cool component surface, and \( F_0 \) is the flux from the cool component at the same point. A change of the continuum slope in the UV band at the various orbital phases, observed by HST, confirms this picture. Parameters \( a \) and \( b \) deduced for each \( \lambda \) are presented in Figure 12.
In the log solution from Table 2. To account for differences between the blackbody observed ones are shown by open symbols. All models are computed for the exposure length. The model fluxes, integrated in the same phase ranges as their disparity indicates the difference of light curve smoothing due to the HST obtained separately from error bars mark exposure length for each point. The light curves at 1650 Å are computed light curves in the same bands (solid and dashed lines). The horizontal (top panel), 1650 Å (middle panel), and 1900 Å (bottom panel) with the parameters for flux correction in corresponding bands are marked in the plot. (A color version of this figure is available in the online journal.)

Figure 12. Comparison of the observed light curves (filled symbols) at 1350 Å (top panel), 1650 Å (middle panel), and 1900 Å (bottom panel) with the computed light curves in the same bands (solid and dashed lines). The horizontal error bars mark exposure length for each point. The light curves at 1650 Å are obtained separately from HST FUV (circles) and NUV (triangles) detectors. Their disparity indicates the difference of light curve smoothing due to the exposure length. The model fluxes, integrated in the same phase ranges as observed ones are shown by open symbols. All models are computed for the cool solution from Table 2. To account for differences between the blackbody and real atmosphere we introduced the parameters a and b (see the text), obtained empirically from comparison of these two observed light curves. The values of parameters for flux correction in corresponding bands are marked in the plot. (A color version of this figure is available in the online journal.)

Figure 13. Line with dots depicts the dependence of the $\chi^2$ value on the total mass of the system. Fixed parameters in the calculations were the temperatures of the components (55 and 160 K, respectively) and $M_{cool}$ (0.54 $M_\odot$). The free parameters were the inclination of the binary orbit $i$, which changed similar to the $\chi^2$ in a range of values shown on the upper axes; and the Roche lobe-filling factors ($f_l$) of both components shown as shaded areas in a range of values marked on the right side axes. The dark shaded area corresponds to Roche lobe-filling factor of the hot component and the light gray to that of the cool component.

Figure 14. Position of the hot component in the temperature–luminosity diagram (filled box) respective to the tracks of hot accreting WDs in the steady-burning approximation (Iben 1982). The bold solid curve shows the high-temperature boundary of the stable-burning strip. The numbers by the tracks are corresponding WD masses in $M_\odot$.
The initial system is so wide that the primary evolves to the AGB unaffected by the presence of the companion. In the first giant branch (FGB)\(^{18}\) and AGB, the system might manifest itself as a symbiotic system with AGB and MS components (Kenyon & Webbink 1984). Owing to the wind mass loss from the system, the separation of the components increases. Both the radius of the primary and the radius of its Roche lobe increase, with the radius of the primary growing faster until the primary overflows its Roche lobe (RLOF) close to the tip of the AGB. Both because the primary at this time has a deep convective envelope and the mass ratio of the components is high, the dynamical mass loss is unavoidable (Hjellming & Webbink 1987) and the shedding of the envelope results in formation of a common envelope (CE) and a reduction of the separation of the components due to angular momentum loss in CE. What remains of the primary after this episode is the more massive component of the core of TS 01. The system remains wide enough so that other component may evolve to become a giant star too and experience RLOF close to the tip of the AGB, forming the current cool component. The matter ejected during the second CE episode is now observed as a PN.

We now present numerical estimates that argue in favor of the feasibility of a scenario such as that just described. In our evolutionary simulations, we use the "rapid evolutionary code" SSE (Hurley et al. 2000) based on the analytical fits to detailed grids of full stellar models. We use the SSE code because detailed evolutionary tracks for low-metallicity stars with \(M < 1 \, M_\odot\) have yet to be computed. Comparison with data for more massive stars (e.g., Weiss & Ferguson 2009) shows that the initial-final mass relations used by us agree with the results of sophisticated, full evolutionary computations to within \(\approx 10\%\) per cent and, hence, qualitatively, the resulting scenario must be robust. We note also, that the results of evolutionary calculations depend heavily on the opacities used for the models.

Stasiecka et al. (2010) estimate that the metallicity of TS 01 ranges from 1/12 to 1/30 of the solar value (taken as \(Z_\odot = 0.014\); Lodders et al. 2009). For our calculations we accepted \(Z = 0.001\) as a proxy to the metallicity of TS 01, since our goal is to demonstrate the possibility of forming a system similar to TS 01, rather than attempt to reproduce precise values for parameters that are still quite uncertain.

The second CE episode, which produced the current cool component, followed RLOF by its precursor close to the tip of AGB. Using SSE, we find that, for \(Z = 0.001\), stars with a ZAMS mass exceeding 0.89 \(M_\odot\) evolve to the tip of AGB in less than 10 Gyr. At the tip of the AGB, a star with \(M_{\text{ZAMS}} = 0.89 \, M_\odot\) has a mass of 0.60 \(M_\odot\) and a core mass of 0.54 \(M_\odot\), which is coincidentally similar to the estimated mass of the cool component in TS 01. Motivated by Figure 13, we adopt a total system mass of 1.39 \(M_\odot\). Given a mass of 0.54 \(M_\odot\) for the cool component, the mass of hot component is then \(\approx 0.85 \, M_\odot\), corresponding to an initial mass of 2.5 \(M_\odot\).

At the tip of AGB, the precursor of the cool component had a radius \(R \approx 140 \, R_\odot\). Using the formula from Eggleton (1983) for the dimensionless radius of the Roche lobe \(r_2\), we estimate that the pre-CE separation of components was about 400 \(R_\odot\). The variation of the separation of components in CE's may be described by the formula suggested by Webbink (1984):

\[
\frac{a_f}{a_0} = \frac{M_c}{M_d} \left[ 1 + \frac{2}{\alpha_{\text{ce}} \lambda_{r_2 L}} \frac{M_2 - M_c}{M_1} \right]^{-1},
\]

where \(M_2\) and \(M_c\) are initial and final masses of mass-losing component (the donor), \(M_1\) is the mass of companion, \(\alpha_{\text{ce}}\lambda\) is the product of efficiency of CE expulsion \(\alpha_{\text{ce}}\) and the structural parameter \(\lambda\) which characterizes binding energy of the donor envelope. \(r_{2L}\) is the fractional Roche lobe radius of the donor. The reduction of the separation from \(a_0 \approx 400 \, R_\odot\) to the current \(a_f \approx 1.3 \, R_\odot\) is possible if \(\alpha_{\text{ce}} \lambda \approx 0.0015\), i.e., is extremely low.

In the stage preceding the CE, the system contained an AGB star and a massive (hot) companion accreting from the wind. In this stage, the system could be identified with a symbiotic star (Tutukov & Yungelson 1976; Kenyon & Webbink 1984; Yungelson et al. 1995; Lü et al. 2006). Accretion reheated WD and resulted initially in unstable and later in stable hydrogen burning at the surface of WD. Energy release by nuclear burning also contributed to the heating of WD.

It is plausible that currently hot component still burns remaining of hydrogen accreted in this stage. During the symbiotic stage, the precursor of the cool component lost about 0.29 \(M_\odot\) via a wind. Accretion from the wind in symbiotic systems is inefficient (~10%; de Val-Borro et al. 2009) and we may safely assume that all mass lost by the donor was lost from the system taking away specific angular momentum of the donor ("Jeans mode of mass ejection") and that the mass of the hot component did not change. Jeans mode of mass ejection has an invariant \(a \times (M_1 + M_2)\) and, hence, the separation of the components in the beginning of the symbiotic stage was \(320 \, R_\odot\). This separation, \(320 \, R_\odot\), is also the separation of components after the first CE stage, which aborted the ascend of AGB by the initially more massive component close to the tip of the AGB. Before the first CE stage, the mass of the star decreased via wind mass loss from 2.5 \(M_\odot\) to 1.29 \(M_\odot\). Its radius at the tip of the AGB was 495 \(R_\odot\). Like for the second RLOF episode, from the condition of RLOF we may estimate that the separation of the components at the beginning of the first RLOF was 1200 \(R_\odot\). The reduction of the separation in the first CE phase from 1200 \(R_\odot\) to 320 \(R_\odot\) implies \(\alpha_{\text{ce}} \lambda \approx 1.5\). The first CE episode could also have been preceded by a symbiotic stage. We again assume that all mass

\(^{18}\)The first giant branch, in which the helium nucleus is formed but not burning yet.
Figure 15. Schematic depicting the evolution of TS 01.

(A color version of this figure is available in the online journal.)

### Table 5

| $M_1$ (M$_\odot$) | $M_2$ (M$_\odot$) | $a$ (R$_\odot$) | Comment |
|------------------|------------------|----------------|---------|
| 2.5              | 0.89             | 770            | ZAMS    |
| 1.29             | 0.89             | 1200           | The end of AGB ascend by the primary, beginning of the first RLOF (CE) |
| 0.86             | 0.89             | 320            | The end of the first CE, $\alpha_{ce} \approx 1.5$, formation of the first WD, beginning of the symbiotic stage |
| 0.86             | 0.60             | 400            | The end of the symbiotic stage; RLOF (CE); ejection of PN, $\alpha_{ce,\lambda} \sim 0.001$ |
| 0.86             | 0.54             | 1.3            | Present state |
| 5.0              | 0.89             | 150            | ZAMS    |
| 5.0              | 0.89             | 150            | The end of FGB ascend by the primary, beginning of the first RLOF (CE) |
| 0.87             | 0.89             | 240            | The end of the first CE, $\gamma \approx 1.2$, formation of He-star evolving into first WD, beginning of the symbiotic stage |
| 0.87             | 0.73             | 260            | The end of secondary evolution in E-AGB; RLOF (CE); ejection of PN, $\alpha_{ce,\lambda} \sim 0.01$ |
| 0.87             | 0.53             | 1.3            | Present state |

**Note.** The upper part of the table shows scenario (I) based on energy balance formalism of Webbink (1984), while the lower part of the table presents scenario (II) based on the angular momentum balance formalism of Nelemans et al. (2000).

lost by the donor was lost from the system via the Jeans mode of mass ejection. We then estimate the initial separation of components as close to $770 \, R_\odot$. We neglect the wind mass loss during the first red giant stage, which is only several $0.01 \, M_\odot$ for $M_0 \simeq 2.5 \, M_\odot$. The numerical data are summarized in the upper part of Table 5 (scenario I) and is presented in a form of a cartoon in Figure 15.

An apparent problem with the suggested scenario is the large difference in $\alpha_{ce,\lambda}$ for the CE stages. While $\alpha_{ce,\lambda} \sim 1$ is typical for WD+MS stars with periods below about 10 days, which are supposed to form via one CE stage and implies that the energy spent on the expulsion of the CE is comparable to the orbital energy of the initial binary (Nelemans & Tout 2005), $\alpha_{ce,\lambda} \sim 0.001$ during the second CE episode appears atypically low. However, CEs remain virtually terra incognita in stellar evolution and we cannot exclude a significant difference in the interaction of the AGB star envelope with an MS or a WD companion, which differ in structure and, most importantly, by two orders of magnitude in radius (whereas the drag force is $\propto R^2$).

An alternative scenario for TS 01 assumes that the present cool component had a precursor with ZAMS mass of $0.89 \, M_\odot$, while the hot component descended from a helium star which was formed by RLOF close to the tip of FGB. For instance, a $5 \, M_\odot$ star has a maximum He-core mass of $0.87 \, M_\odot$ which, presumably, evolves into a CO WD of the same mass. 19 Thus, the

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19 We set the mass of WD equal to the mass of its He-star precursor, thus implicitly neglecting the possibility of reexpansion of the He-star after exhaustion of helium in its core. Such an expansion with formation of a shallow CE and almost negligible mass loss was discovered by Iben & Tutukov (1985) for solar metallicity stars, but its possibility was never explored for non-solar metallicities.
The initial system could contain a 5 $M_\odot$ component and a 0.89 $M_\odot$ component and after the 1st CE to become a (0.87+0.89) $M_\odot$ system. If 5 $M_\odot$ star filled Roche lobe close to the tip of FGB when it radius was close to 80 $R_\odot$, prior to RLOF separation of components had to be close to 150 $R_\odot$.

If the precursor of the cool component was an AGB star, the smallest radius with which it could overfill its Roche lobe at E-AGB was $\approx 100$ $R_\odot$. At this moment the total mass of the star was 0.73 $M_\odot$, the mass of the core – 0.53 $M_\odot$, and from the RLOF condition we obtain that the separation of the stars was $\approx 260$ $R_\odot$. In the second CE the separation decreased from 260 $R_\odot$ to 1.5 $R_\odot$ by ejection of 0.2 $M_\odot$. This is possible if $\alpha_{ce} \lambda \approx 0.1$, i.e., an order of magnitude larger than in the first scenario.

If we account for Jeans-mode mass loss by the precursor of the cool component we obtain that, after the first CE, the separation of components was close to 240 $R_\odot$. Thus, we arrive to an apparent controversy: in the suggested scenario, in the first CE episode, the separation of the components had to increase from 150 to 240 $R_\odot$.

However, it was noticed by Nelemans et al. (2000) and later confirmed by Nelemans & Tout (2005) that using Equation (1) for the description of the outcome of unstable mass exchange between a giant and an MS star often does not allow one to reproduce well measured parameters of many post-CE binaries. As an alternative, Nelemans et al. (2000) suggested to estimate the post-CE separations of components using an equation for angular momentum balance:

$$J_i - J_f = \gamma J_i \frac{\Delta M}{M_{tot}} \tag{2}$$

Here $J$ is the orbital angular momentum, subscripts i and f denote the initial and final values of the momentum, $\Delta M$ is the mass lost from the system (the envelope of the donor), and $M_{tot}$ is total initial mass of the system. Thus, a single parameter $\gamma$ describes the fraction of initial specific orbital angular momentum of the binary taken away by outflowing matter. This “$\gamma$-formalism” leads to

$$\frac{a_i}{a_0} = \left( \frac{M_1}{M_2} \right)^{2} \left( \frac{M_c + M_2}{M_{tot}} \right) \left( 1 - \gamma \frac{\Delta M}{M_{tot}} \right)^{3} \tag{3}$$

Here $M_c$ is the mass of the core of the mass-losing component. An increase of the separation during the CE from 150 to 240 $R_\odot$ is possible if $\gamma \approx 1.2$. Rather similar combinations of $\gamma$ for the first CE and $\alpha_{ce} \lambda$ for the second one were found for some systems studied by Nelemans & Tout (2005, see their Figures 1 and 5).

### 4.2. Common Envelope Remnant versus Single Star Evolution through post-AGB Phase

Ejection of a CE definitely differs from formation of a PN by the usually assumed superwind mechanism. In that context, it is interesting to compare parameters of the cool star deduced here with the evolutionary models for post-AGB stars. Given that the cool component of TS01 nearly fills its Roche lobe and that it is currently contracting, it has only recently terminated the phase of CE evolution. The structure and mass of its envelope might be very different from that of a single star passing through the early epochs of PN nucleosynthesis. Here we compare the derived parameters of the cool component of TS 01 with two sets of models of remnants of single stars with initial masses of 1.0 $M_\odot$ (lower progenitor masses are not available in the literature). Based on estimated abundances, we selected the models $M = 0.623 M_\odot$, $Z = 0.001$ Vassiliadis & Wood (1994), and $M = 0.547 M_\odot$, $Z = 0.0005$ Weiss & Ferguson (2009).

These models agree well regarding the time dependence of heating of the core of a post-AGB star (lower right panel of Figure 16). TS 01 has $T_{eff}$ similar to them at the age of $\approx 6000$ yr. This age estimate is in a good agreement with the age deduced from the expansion velocity and distance to the PN (Stasińska et al. 2010).

Compared to the most modern and the closest in mass model of Weiss & Ferguson (2009), the nucleus of TS 01 is slightly more compact (by 0.05 dex) and significantly (by more than 0.3 dex) less luminous. Since the main source of luminosity of post-AGB stars is hydrogen burning, this may mean that CE remnants may have less massive H/He envelopes around degenerate cores than their post-AGB counterparts.

This comparison clearly indicates that evolution in CEs might alter evolution of stars in close binary systems compared to single stars and a more complete analysis of TS01 is warranted than can be made with single star models.

### 4.3. TS 01 and SNe Ia

The evolutionary path suggested for TS 01 includes a stage of a symbiotic star which is considered as one of the routes to SN Ia (e.g., Tutukov & Yungelson 1976; Iben & Tutukov 1984; Munari & Renzini 1992). However, conditions in symbiotic systems are not favorable for an efficient accumulation of matter by the WD components. Accretion from the wind typically allows only several percent of the mass lost by the donor to be accreted. In the numerical scenario above, the maximum mass-loss rate by the progenitor of the cool component estimated by means of SSE is close to $2 \times 10^{-7}$ $M_\odot$ yr$^{-1}$. This means that for about 10 Gyr the WD (hot) component stays in the regime of unstable thermonuclear burning (of novae eruptions; Nomoto 1982) and
Using Bondi & Hoyle (1944) formalism for wind accretion, 2007). Then accretion efficiency may become close to 100%. Pulsations and still remains slow (Podsiadlowski & Mohamed or if the stellar wind is pumped close to the Roche lobe by the tendency of better fit to the observed data with increase of total mass of the component, the matter could inflow onto the equatorial regions instead of accumulating mass it may erode. Conditions for accretion “improve” if the accretor is located in the zone of acceleration of the stellar wind, which requires the proximity of the donor surface to the Roche lobe (Yungelson et al. 1995), or if the stellar wind is pumped close to the Roche lobe by pulsations and still remains slow (Podsiadlowski & Mohamed 2007). Then accretion efficiency may become close to 100%. Using Bondi & Hoyle (1944) formalism for wind accretion, accounting for possible location of the accretor in the wind acceleration zone and taking accretion rate limits for stable hydrogen burning after Nomoto (1982), we estimate that the system could accrete steady for the last several 100,000 yr prior to CE and accumulate only several 0.01 $M_\odot$. In a more general context, the circumstances listed above prevent symbiotic stars from being efficient progenitors of SN Ia and the estimated rate of occurrence of SN Ia in these systems is only $\sim 10^{-6}$ yr$^{-1}$ on a Galactic scale (e.g., Yungelson 2005).

For a fraction of time between Novae eruptions and in steady-burning regime the system can manifest itself as an SSS (e.g., van den Heuvel et al. 1992; Truran & Glasner 1995; Yungelson et al. 1996). Note that, during the stage of accretion onto the current hot component, the matter could inflow onto the equatorial regions of the dwarf while it outflows from the polar regions. The “bars” seen in TS 01’s nebular shell (Stasiński et al. 2010) may be the remnants of jets that once existed in the system.

Figure 17 shows the positions of double-degenerate systems with known parameters in the $M_{\text{sdB}}-P_{\text{orb}}$ plane. As well, positions of several sdB stars with WD companions are shown. The latter systems will turn into double degenerates after completion of helium burning in sdB stars. Thus, its short orbital period of 3.92 hr and its total mass close to the Chandrasekhar mass makes TS 01 very promising candidate progenitor for an SN Ia in the double-degenerate scenario for these events (Tutukov & Yungelson 1981; Iben & Tutukov 1984; Webbink 1984). For instance, the merger of components will occur in $\approx 660$ Myr in the first evolutionary scenario suggested above and in $\approx 1.2$ Gyr in the second scenario. The only “competitor” to TS 01 is sdB+WD system KPD 1930+2752 with orbital period 2.28 hr, $M_{\text{sdB}} = 0.45-0.52 M_\odot$, $M_{\text{tot}} = 1.36-1.48 M_\odot$ (Geier et al. 2007). In the latter system, subdwarf star will turn into a WD in $(220-140)$ Myr, see Yungelson (2008) for estimates of lifetime of sdB stars. It will take two WD several tens of Myr more to merge. Favourable conditions for central carbon ignition may come to fruition just in systems with low mass ratios of components (Yoon et al. 2007), like TS 01 and KPD 1930+2752.

5. CONCLUSIONS

After a decade of intense study, we have achieved a good understanding of an object whose discovery spectrum was misidentified and incomprehensible in 1997. Since then, the object has been observed at practically all wavelengths with the help of the most advanced instruments. This paper accompanies Stasińska et al. (2010), which focuses upon the chemical composition and ionization state of TS 01’s nebular shell. Here, we focus on the nature of the close binary nucleus of the PN.

TS 01 is one of the shortest period systems among the double-degenerate or pre-double-degenerate systems, with an orbital period of 3.924 hr This fact would not have caused confusion if the older of the components were significantly cooler than the core of the star that most recently ejected its envelope to form the current PN. However, observations and analysis clearly demonstrate that TS 01’s nucleus is comprised of two compact stars, both extremely hot and thus, both being sources of ionization for the nebula. This unusual phenomenon created confusion and misinterpretation of the object in the past. Nevertheless, the correct understanding of the ionization source does not change the essence of those previous interpretations. TS 01 remains a PN with a record low oxygen abundance (Stasińska et al. 2010).

According to our scenario, TS 01 evolved through two CE episodes. In the current stage we are observing the remainders of the second CE as a PN. The core of the envelope-shedding post-AGB star is in the process of contraction and heating up. At the present time, it nearly fills its Roche lobe and has an ellipsoidal shape. Before the last CE episode, the more massive component, which became a WD earlier, underwent a period during which it accreted mass at a high rate and burned hydrogen steady. Since then it stays close to the temperatures range typical for SSS. Its properties make TS 01 one of the softest X-ray sources ever, similar to Lin 358 (Orio et al. 2007).

The parameters of the binary system were deduced using a wealth of information and via three independent routes. Although, each of these methods requires its own assumptions and each alone produces ambiguous results, in combination, they converge to values with unusual precision. Using the spectral energy distribution, from the far infrared to X-rays, the light and RV curves, and by fitting atmospheric models to the stellar absorption features of the cool component, we find that the cool component has a mass of $0.54 \pm 0.2 M_\odot$, an average $T_{\text{eff}}$ of 58,000 ± 3000 K, a mean radius of 0.43 ± 0.3 $R_\odot$, and $\log g = 5.0 \pm 0.3$. The cool component nearly fills its Roche lobe. The temperature and gravity over the surface of the cool component are not homogeneous.
The chemical composition of the cool component from atmosphere model fitting was determined as: \(12 + \log \text{He}/\text{H} = 10.95\) and \(12 + \log \text{C}/\text{H} = 7.20\), with an uncertainty of about 0.3 dex, and upper limits 12 + \log \text{N}/\text{H} < 6.92 and 12 + \log \text{O}/\text{H} < 6.80. Overall, the agreement with the abundances found in the nebula by Stasińska et al. (2010) is very good, except for the carbon abundance, which is found to be higher in the nebula for a reason yet not understood.

The parameters for the hot component are less certain. It is fairly clear that the spectral energy distributions of real stars at such high temperatures depart from that of a blackbody. The range of temperatures that we determined for the hot component spans 160–200 kK. It seems that the real object acts like a 180–200 kK blackbody in the X-ray range but appears as a 160 kK blackbody in the UV/optical range. Uncertainty in its temperature leads to uncertainty in its size, but it is obvious from our calculations that the hot component is larger than normal for a WD, \(R_{\text{hot}} > 0.1 R_\odot\), and is probably bloated as a result of intense accretion in the recent past. However, we have indirect information on the hot component through photoionization modeling by reproducing the intensities of the lines emitted by the nebula (Stasińska et al. 2010). We estimate the distance to the object as \(\sim 21\) kpc, and our most reasonable luminosity estimate for the X-ray component is \(\sim 10^4 L_\odot\), appropriate for an SSS.

The total mass of the binary is very close to Chandrasekhar limit. This makes TS 01 one of the best of the known candidates for the progenitor of a type Ia supernova.

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