Learning Semantic Correspondence with Sparse Annotations

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Abstract. Finding dense semantic correspondence is a fundamental problem in computer vision, which remains challenging in complex scenes due to background clutter, extreme intra-class variation, and a severe lack of ground truth. In this paper, we aim to address the challenge of label sparsity in semantic correspondence by enriching supervision signals from sparse keypoint annotations. To this end, we first propose a teacher-student learning paradigm for generating dense pseudo-labels and then develop two novel strategies for denoising pseudo-labels. In particular, we use spatial priors around the sparse annotations to suppress the noisy pseudo-labels. In addition, we introduce a loss-driven dynamic label selection strategy for label denoising. We instantiate our paradigm with two variants of learning strategies: a single offline teacher setting, and mutual online teachers setting. Our approach achieves notable improvements on three challenging benchmarks for semantic correspondence and establishes the new state-of-the-art. Project page: https://shuaiyihuang.github.io/publications/SCorrSAN.

Keywords: semantic correspondence, pseudo-label, sparse annotations

1 Introduction

Estimating pixel-wise correspondence between images is a fundamental task in computer vision applications. Correspondences like stereo disparities [47] and optical flow [20] are widely used for applications such as surface reconstruction and video analysis [3,8]. Recently, such instance-level dense correspondence has been generalized to semantic correspondence, which, given a pair of images, aligns the object instance from the first image to the one of the same category in the second image [44,45,28,22,40,42,24,52]. It has attracted growing attention due to its practical use in segmentation, style-transfer, and image editing [30,5,33,7,26,18]. However, background clutter, intra-class variations, viewpoint changes, and particularly the severe lack of annotations make it an extremely challenging task.
Due to the high cost of dense annotation, the semantic correspondence task only provides sparse keypoint annotations in the supervised setting [42,35,36,31] as shown in Fig. 1. In this paper, we are motivated by how to better utilize the limited supervision. Specifically, we explore the techniques to generate pseudo-labels. However, due to the inevitably noisy effect of pseudo-labels, filtering out noisy pseudo-labels remains a challenging problem. Our key observation is that sparse keypoint annotations and their neighborhood encode rich semantic information. By utilizing this spatial prior, one can seek reliable pseudo-labels that are more likely in the foreground region of interest.

To this end, we propose a novel teacher-student framework to cope with label sparsity. The teacher model is trained with sparse keypoint annotations to generate dense pseudo-labels. To improve pseudo-labels quality, we propose (a) using the sparse annotations as spatial prior to suppress the noisy pseudo-labels, and (b) loss-driven dynamic label selection. To train the models, we propose two variants of our strategy: (1) a single offline teacher with an online student, and (2) two online teachers that learn from each other. Both variants lead to substantial performance improvements over the state-of-the-art.

We instantiate our novel learning strategy based on our proposed simple, yet effective network architecture for semantic correspondence. The proposed network comprises three modules: (a) a feature extractor equipped with our efficient spatial context encoder, (b) a parameter-free correlation map module, and (c) a flow estimator with our designed high-resolution loss.

The contributions are summarized as follows:

- We propose a simple, yet effective model for semantic correspondence without any transformer or 4D-conv for correlation refinement. The key ingredients are an efficient spatial context encoder and a high-resolution loss.
- We introduce a novel teacher-student learning paradigm to enrich the supervision guidance when only sparse annotations are available. Two key
techniques are a novel spatial-prior based label filtering and a loss-driven
dynamic label selection strategy for high-quality pseudo-label generation.
– Our novel learning strategy is simple to implement, and achieves state-of-
the-art results with good generalization performance on three semantic cor-
respondence benchmarks, demonstrating the effectiveness of our method.

2 Related Work

2.1 Semantic Correspondence

Conventional approaches for semantic correspondence mostly employ hand-crafted
features together with geometric models [37,51,49]. These methods establish cor-
respondences across images via energy minimization. SIFT Flow [37] pioneers
the idea of finding correspondences across similar scenes with SIFT descriptors.
Ham et al. [10] utilize object proposals as the matching primitives and establish
correspondence via HOG descriptors. Those methods often have difficulty deal-
ing with background clutter, intra-class variations, and large viewpoint changes
due to the lack of semantics in features.

Recently, deep CNN-based methods have been widely used in semantic cor-
respondences due to their powerful representations. Early methods formulate
semantic correspondence as a geometric alignment problem, with a major focus
on developing robust geometric models [19,44,27]. Rocco et al. [44,45] propose
a two-stage CNN architecture for regressing image-level transformation param-
eters, while other efforts regress local translation fields [27,26,29]. More recent
works tend to formulate semantic correspondence as a pixel-wise matching prob-
lem and cast it as a classification problem. Among these works, there are tech-
niques focusing on developing powerful feature representations [22,40,42], corre-
lation map filtering with 4D/6D-conv or transformers [35,38,6,39,18], effective
correspondence readout [32], and different levels of supervision [36,21,53]. How-
ever, none of these aforementioned methods have explicitly approached the task
of dense semantic correspondence from the perspective of sparse annotations.

2.2 Teacher-Student Learning

Teacher-student framework has been widely used in semi-supervised learning
(SSL) [48,54,50,34,13], where the predictions of the teacher model on unlabeled
samples serve as pseudo-labels to guide the student model. Teacher-student
framework also plays an important role in knowledge distillation [17,4,57,16,60],
where knowledge from a larger teacher model can be transferred into a smaller
student model without loss of validity. Recently, Xin et al. [36] extend teacher-
student to semantic correspondence, where they distill knowledge learned from
a probabilistic teacher model on synthetic data to a static student model with
unlabeled real image pairs. In contrast, we directly learn from real image pairs
labeled with sparse keypoints, and focus on addressing the label sparsity chal-
lenge via Siamese teacher-student network design [2]. Note that we tailor teacher-
student learning specifically for the dense prediction task of semantic correspon-
dence, where we conduct pixel-level semi-supervised learning within an image
and generate pseudo-labels for unlabeled pixels, while most existing work focus on image-level semi-supervised learning.

3 Model Architecture

Semantic correspondence establishes dense correspondences between a source image $I_a$ and a target image $I_b$. We adopt a typical CNN-based method which computes a correlation map between the convolution features of two images, based on which a dense flow field is predicted as the final output. We additionally encode spatial context efficiently to compute high-quality correlation map and develop a novel teacher-student learning strategy to cope with label sparsity.

This section introduces our simple and powerful semantic correspondence framework. As depicted in Fig. 2, our framework comprises of three main modules: (1) a sparse spatial context feature extractor that encodes context information efficiently (Sec. 3.1), (2) a correlation operator to compute the correlation map between two convolution features (Sec. 3.2), and (3) a flow estimation operator with high-resolution loss (Sec. 3.3).

3.1 Efficient Spatial Context Encoder

Taking the conv features of the image pairs as the input, the first component of our network is an efficient spatial context encoder that incorporates spatial context into conv features. Recent methods adopt the self-similarity based descriptor to encode spatial context [22,35]. However, the time complexity of the self-similarity grows quadratically with respect to the kernel size of the self-similarity descriptor due to dense sampling patterns they used [22,35]. Inspired by the recent success of sparse attention on reducing the computational cost of non-local operation [23,58,14,59], we propose a spatial context encoder based
on sparse sampling patterns, which efficiently encodes context information and reduces the time complexity from quadratic to linear.

As shown in Fig. 2(b), at location \((i, j)\), its spatial context descriptor \(s_{(i,j)} \in \mathbb{R}^{4K}\) is a self-similarity vector, where \(K\) is the self-similarity operator kernel size. It is computed between its own feature vector \(z_{(i,j)} \in \mathbb{R}^{d_z}\) and its 4\(K\) neighboring feature vectors, where the neighbors are in its criss-cross and diagonal directions in an fixed order. In contrast to dense sampling patterns [22,35], our sparse sampling patterns reduce the time and space complexity for computing spatial descriptors from \(O(K^2)\) to \(O(K)\).

To combine spatial context and conv features, we employ a simple fusion step to generate the final context-aware semantic feature map \(G\) following [22]. Concretely, we concatenate \(z_{(i,j)}\) and \(s_{(i,j)}\) and feed the result into a linear transformation with parameter \(W \in \mathbb{R}^{(d_z+4K) \times d_g}\) followed by a ReLU operation, resulting in a context-aware semantic feature vector \(g_{(i,j)} \in \mathbb{R}^{d_g}\). We add subscripts to represent the context-aware semantic feature map \(G \in \mathbb{R}^{d_g \times h_a \times w_a}\) for the image \(I_a\) and \(G_b \in \mathbb{R}^{d_g \times h_b \times w_b}\) for the image \(I_b\), resp., where \(h_b, w_b\) (resp. \(h_a, w_a\)) is the spatial size of \(G_b\) (resp. \(G_a\)).

### 3.2 Correlation Map Computation

We compute a 4D correlation map from the context-aware semantic feature maps \(G_a, G_b\) and filter it with the mutual nearest neighbor module [46]. We denote the resulting 4D correlation map as \(C \in \mathbb{R}^{h_a \times w_a \times h_b \times w_b}\).

We propose to learn a high-resolution correlation map for high-quality dense matching in contrast to learning correspondence in stride16 [22,45]. We upsample the correlation map \(C\) (4 times) instead of upsampling the feature maps for memory efficiency. We denote the resulting upsampled correlation map as \(C = \mathcal{U}(C), \quad C \in \mathbb{R}^{H_a \times W_a \times H_b \times W_b}\),

where \(H_a, W_a, H_b,\) and \(W_b\) are the upsampled spatial sizes, \(\mathcal{U}\) is the upscale operation. Note that we achieve high performance with single layer feature, while DHPF [42] requires multi-layer features with higher complexity.

### 3.3 Flow formation and High-resolution loss

To obtain differentiable flow, we adopt the kernel soft-argmax operator [32] to transform the upsampled correlation map \(C\) into dense semantic flow \(\hat{f}\) as below:

\[
\hat{f} = \mathcal{S}(C), \quad \hat{f} \in \mathbb{R}^{2 \times H_b \times W_b}
\]

where \(\mathcal{S}\) is the kernel soft-argmax operator without any learnable parameters, \(\hat{f}\) is the predicted semantic flow in the direction of the target to source.

During training, as we only have sparse keypoint labels, the ground-truth flow \(f^{gt} \in \mathbb{R}^{2 \times H_b \times W_b}\) have valid values only at labeled positions. We use a sparse
Fig. 3. Sparse Label Densification with Teacher-Student Learning. (a) Our Teacher-Student Learning Pipeline. Solid lines stand for Single Offline Teacher, with additional dashed lines standing for Mutual Online Teacher. (b) Illustration of Label Mask Dilation. Please refer to Sec. 4 for more details. Best viewed in color.

Fig. 3. Sparse Label Densification with Teacher-Student Learning. (a) Our Teacher-Student Learning Pipeline. Solid lines stand for Single Offline Teacher, with additional dashed lines standing for Mutual Online Teacher. (b) Illustration of Label Mask Dilation. Please refer to Sec. 4 for more details. Best viewed in color.

binary label mask $M \in \mathbb{R}^{H_b \times W_b}$ to indicate valid positions with ground-truth labels as below:

$$M(p) = \begin{cases} 1 & \text{if } p \text{ is labeled,} \\ 0 & \text{otherwise,} \end{cases}$$

where $p$ is the position index in $f^{gt}$.

Given $M$, the objective is then defined as the L2 norm between the predicted flow and the ground-truth flow at labeled subpixel positions:

$$L^{gt}(p) = \|f(p) - f^{gt}(p)\|_2 \cdot M(p)$$

where $L^{gt}(p)$ is the ground-truth loss at position $p$. It is worth noting that our network does not involve any 4D-conv or transformer for correlation refinement [6,22], but as shown later it achieves high performance thanks to our efficient spatial context encoder and high-resolution design.

4 Learning with Sparse Annotations

While our network design enables us to encode spatial context efficiently and utilize high-resolution correlation maps, the sparsely-annotated keypoint pairs (8 on average on PF-PASCAL [10]) greatly hinder the learning of the dense matching model. We address this with a novel teacher-student learning framework which we will elaborate below.
Our goal is to enrich the supervision when only sparse annotations are provided, as shown in Fig. 3. We first densify the sparse labels with a teacher-student paradigm (Sec. 4.1). Then we introduce two novel techniques to denoise the generated pseudo-labels (Sec. 4.2): (a) leveraging spatial-priors and (b) loss-driven dynamic label selection. Finally, we investigate two variants of the proposed learning paradigm (Sec. 4.3).

4.1 Sparse Label Densification via Teacher-Student Learning

To enrich the sparse supervision signals, we generate dense pseudo-labels for unlabeled region via a teacher-student paradigm, which consists of a student model \( F_s \) and a teacher model \( F_t \). The teacher model \( F_t \) trained with sparse annotations generates dense flows \( \hat{f}_t \), providing pseudo-labels \( f_{pseudo} \) for the student model \( F_s \). Formally,

\[
f_{pseudo} = F_t(I_a, I_b), \quad f_{pseudo} \in \mathbb{R}^{2 \times H_b \times W_b}.
\]

(5)

Then, the optimization objective \( L_s(p) \) for the student \( F_s \) is a combination of the ground-truth loss \( L_{gt}(p) \) and a dense pseudo-label loss \( L_{pseudo}(p) \) calculated as follows:

\[
L_s(p) = L_{gt}(p) + \lambda L_{pseudo}(p)
\]

(6)

\[
L_{gt}(p) = \| \hat{f}_s(p) - f_{gt}(p) \|_2 \cdot M(p)
\]

(7)

\[
L_{pseudo}(p) = \| \hat{f}_s(p) - f_{pseudo}(p) \|_2
\]

(8)

where \( \hat{f}_s \in \mathbb{R}^{2 \times H_t \times W_t} \) is the predicted flow of the student model \( F_s \) given \( I_a \) and \( I_b \), \( \lambda \) is the scale hyper-parameter, \( p \) indexes the positions in \( \hat{f}_s \).

4.2 High Quality Pseudo-label Generation

The dense pseudo-labels generated by the teacher model are inevitably unreliable and inaccurate for supervision. To filter out erroneous pseudo-labels, we use: (a) label filtering based on spatial priors, and (b) loss-driven dynamic label selection.

Spatial-prior Based Label Filtering. Our key insight is that, as the annotated keypoints are in the object foreground region, we are able to suppress noisy background pseudo-labels by exploiting the spatial-smoothness prior of the semantic correspondence in the neighborhood of the sparse keypoints. Motivated by this, we generate a densified binary label mask \( \hat{M} \) via dilating the sparse label mask \( M \) as follows, which will be used for label filtering:

\[
M = M * K
\]

(9)

\[
M(p) = \begin{cases} 
1 & \text{if } \hat{M}(p) > 0 \\
0 & \text{otherwise}
\end{cases}
\]

(10)
where * is a convolution operator with zero padding, $K \in \mathbb{R}^{k \times k}$ is a kernel filled with one with $k$ as the kernel size. Note that dilation here refers to expanding the existing foreground region in $M$. Compared with using CAM [62] or uncertainty estimation [36], our proposed label filtering technique is easy to implement and utilizes the spatial prior around the sparse annotations.

Given the dilated label mask $\hat{M}$, the pseudo-loss $\hat{L}_{s}^{\text{pseudo}}(p)$ for the student model is calculated as below:

$$\hat{L}_{s}^{\text{pseudo}}(p) = \|\hat{f}_{s}(p) - f_{s}^{\text{pseudo}}(p)\|_{2} \cdot \hat{M}(p).$$

(11)

where $p$ indexes the positions. In this way, we are able to significantly suppress noisy background pseudo-labels as shown in Sec 5.3.

**Loss-driven Dynamic Label Selection.** While many background pseudo-labels can be filtered out by our dilated label mask, some noisy labels still exist due to inaccurate predictions from the teacher model. To further filter out inaccurate labels, we introduce a loss-driven label selection strategy following the small-loss principle [11]. Denoting $R$ as the ratio of pixels being selected, we choose the pixel set $P$ on the foreground region in $\hat{M}$ with the smallest loss as below:

$$P = \arg\min_{p \in \hat{D} : |D| \geq R(T)N_{\hat{M}}} \sum_{p \in \hat{D}} \hat{L}_{s}^{\text{pseudo}}(p)$$

(12)

$$\hat{D} = \{p \mid \hat{M}(p) = 1\}$$

(13)

where $R(T)$ controls the selection percentage in training epoch $T$, $p$ indexes the positions, $\hat{D}$ is a collection of foreground positions in the dilated label mask $\hat{M}$, $N_{\hat{M}}$ is the total number of non-zero positions in $\hat{M}$.

Hence the final optimization objective $L_{s}$ for the student model $F_{s}$ over an image pair is a combination of the sparse ground-truth loss $L_{s}^{\text{gt}}$ at labeled positions $G = \{p \mid M(p) = 1\}$ and the dense pseudo loss $L_{s}^{\text{pseudo}}$ at selected positions $P$ as below:

$$L_{s} = L_{s}^{\text{gt}} + \lambda L_{s}^{\text{pseudo}}$$

(14)

$$L_{s}^{\text{pseudo}} = \frac{1}{|P|} \sum_{p \in P} \hat{L}_{s}^{\text{pseudo}}(p)$$

(15)

$$L_{s}^{\text{gt}} = \frac{1}{|G|} \sum_{p \in G} L_{s}^{\text{gt}}(p)$$

(16)

### 4.3 Variants of Teacher-Student Learning

To investigate the optimization strategy of our proposed teacher-student learning, we propose two variants of our learning strategy, including (a) single offline teacher, and (b) mutual online teachers, which are detailed below.
Single offline Teacher (ST). This variant consists of two learning stages. Specifically, we first learn a baseline network, which acts as the teacher model, given spare ground-truth annotation only. In the second stage, the pseudo-labels are generated by the fixed teacher network as described in Sec. 4.1 and Sec. 4.2. Given the enriched supervision, we then train the student model from scratch, which is used for the inference stage finally.

Mutual online Teacher (MT). Inspired by the recent advances in multi-view learning [1,55], we additionally explore a one-stage variant with two mutual online teachers which learn from scratch. We simultaneously train two networks of the same architecture, each of which takes predictions from the other network as the pseudo-labels for optimization. These two networks can learn knowledge of correspondence with enriched pseudo-labels from each other. The one with a higher validation performance is selected for the inference stage.

Specifically, we maintain two networks $F_s$ and $F_t$ of the same architecture. The network $F_t$ (resp. $F_s$) provides its predicted flow $\hat{f}_t$ (resp. $\hat{f}_s$) as the pseudo-label $f_{pseudo}^s$ (resp. $f_{pseudo}^t$) for the peer network $F_s$ (resp. $F_t$). Both networks use the shared dilated label mask $\hat{M}$ for label filtering. For each model, the pseudo-loss filtered by dilated label masks is described as below:

\[
\hat{L}_{pseudo}^s(p) = \| \hat{f}_s(p) - f_{pseudo}^s(p) \|_2 \cdot \hat{M}(p) \tag{17}
\]

\[
\hat{L}_{pseudo}^t(p) = \| \hat{f}_t(p) - f_{pseudo}^t(p) \|_2 \cdot \hat{M}(p), \tag{18}
\]

where $p$ indexes the position, $f_{pseudo}^s$ (resp. $f_{pseudo}^t$) equals to $\hat{f}_t$ (resp. $\hat{f}_s$). $\hat{L}_{pseudo}^s(p)$ and $\hat{L}_{pseudo}^t(p)$ will then go through the dynamic label selection procedure as described in Sec. 4.2 to compute pseudo-label loss $L_{pseudo}^s$ and $L_{pseudo}^t$, respectively. The final optimization objective for each model is a combination of sparse ground-truth loss and pseudo loss as below:

\[
L_s = L_{gt}^s + \lambda L_{pseudo}^s \tag{19}
\]

\[
L_t = L_{gt}^t + \lambda L_{pseudo}^t \tag{20}
\]

5 Experiments

We evaluate our method on the supervised semantic correspondence task by conducting comprehensive experiments on three public benchmarks: PF-PASCAL [10], PF-WILLOW [9], and SPair-71k [41]. In the following sections, we first elaborate on the implementation details of our proposed method in Sec. 5.1, and follow that with the quantitative and qualitative comparison with prior state-of-the-art (SOTA) competitors in Sec. 5.2. Then, we provide ablation studies and comprehensive analysis in Sec. 5.3. For more detailed results and analysis, we refer readers to the supplementary material.
Table 1. Comparison with SOTA methods on SPair-71k [41]. Per-class and overall PCK ($\alpha_{bbox} = 0.1$) results are shown in the table. Numbers in bold indicate the best performance and underlined ones are the second best. All models in this table use ResNet101 as the backbone. * Sup. denotes the type of supervision. † means the backbone is finetuned. ‡ means ground truth bbox used.

| Sup. | Methods     | aero | lake | bird | boat | bottle | bus | car | cat | cow | dog | horse | mbike | person | plant | sheep | train | tv  | all |
|------|-------------|------|------|------|------|--------|-----|-----|-----|-----|-----|------|-------|--------|-------|-------|-------|----|-----|
| self | CNNGeo [44] | 23.4 | 16.7 | 40.2 | 14.3 | 36.4   | 27.7| 26.0| 32.7| 12.7| 27.4| 22.8 | 13.7  | 20.9   | 21.0  | 17.5  | 10.2  | 30.8 | 34.1 | 20.6 |
|      | A2Net [19]  | 22.6 | 18.5 | 42.0 | 16.4 | 37.9   | 27.8| 20.5| 35.6| 13.3| 29.6| 24.3 | 16.0  | 21.6   | 22.6  | 19.0  | 13.5  | 31.4 | 36.5 | 22.8 |
|      | WeakAlign [45] | 22.2 | 17.6 | 41.0 | 15.1 | 38.1   | 27.4| 27.2| 31.8| 12.8| 26.8| 22.6 | 14.2  | 20.0   | 22.2  | 17.9  | 10.4  | 32.2 | 35.1 | 20.9 |
|      | NCNet [46]  | 17.9 | 12.2 | 32.1 | 11.7 | 29.0   | 19.9| 16.1| 39.2| 9.9 | 23.9| 18.8 | 15.7  | 17.4   | 15.9  | 14.8  | 9.6   | 32.2 | 35.1 | 20.9 |
|      | trn-none / HPF [40] | 25.2 | 18.9 | 52.1 | 15.7 | 38.0   | 22.8| 19.1| 52.9| 17.9| 33.0| 32.8 | 20.6  | 24.4   | 27.9  | 21.1  | 15.9  | 31.5 | 35.6 | 28.2 |
|      | val-strong SCOT [38] | 34.9 | 20.7 | 63.8 | 21.1 | 43.5   | 27.3| 21.3| 63.1| 20.0| 42.9| 42.5 | 31.1  | 29.8   | 35.6  | 27.7  | 24.4  | 48.4 | 40.8 | 35.6 |
|      | strong DHPF [42] | 38.4 | 23.8 | 68.3 | 18.9 | 42.6   | 27.9| 20.1| 61.6| 22.0| 46.9| 46.1 | 33.5  | 27.6  | 40.1  | 27.6  | 28.1  | 49.5 | 46.3 | 37.3 |
|      | PMD [36]    | 38.5 | 23.7 | 60.3 | 18.1 | 42.7   | 27.6| 26.0| 60.6| 14.0| 54.0| 41.8 | 34.6  | 27.0  | 25.2  | 22.1  | 29.9  | 70.1 | 42.8 | 37.4 |
|      | MMNet* [61] | 49.6 | 29.3 | 68.7 | 29.7 | 45.3   | 48.4| 39.5| 64.9| 28.3| 60.5| 56.1 | 46.0  | 38.3  | 44.3  | 39.9  | 34.1  | 72.2 | 55.5 | 46.3 |
|      | CATs* ‡ [6] | 52.0 | 34.7 | 72.2 | 34.3 | 49.9   | 57.5| 43.6 | 66.5 | 24.4 | 63.2| 56.5 | 52.0   | 46.7  | 43.0  | 33.6  | 72.6  | 59.0 | 49.9 |
|      | PMNC* [31]  | 54.1 | 35.9 | 74.9 | 36.5 | 48.8   | 40.0| 72.6| 21.1 | 67.6| 58.1 | 50.4  | 40.1  | 54.1  | 43.3  | 35.7  | 74.5 | 59.9 | 50.4 |
|      | Ours (ST)*  | 56.9 | 37.0 | 76.2 | 33.9 | 50.1   | 51.7| 42.4 | 69.0 | 47.7 | 51.6 | 47.8  | 47.8   | 48.8  | 60.3  | 77.7  | 69.7 | 55.3 |
|      | Ours (MT)*  | 57.1 | 40.3 | 78.3 | 38.1 | 51.8   | 57.8| 47.1 | 67.9 | 25.2 | 71.3 | 63.9 | 49.3  | 54.3  | 47.8  | 48.8 | 60.3 | 77.7 | 69.7 |

5.1 Implementation Details

Datasets. SPair-71k is a newly-released challenging and largest-scale benchmark [41]. There are keypoint-annotated 70,958 image pairs with large viewpoint and scale variation in diverse scenes. SPair-71k [41] is a reliable test bed for studying real problems of semantic matching. PF-PASCAL dataset [10] contains 1351 image pairs with limited variability and scale, which is approximately split into 700, 300, and 300 pairs for train, val, and test set, resp. PF-WILLOW [9] dataset consists of 900 image pairs of 4 categories, which is a widely-used benchmark for the verification of generalization ability.

Evaluation Metric. In line with prior work, we report the percentage of correct keypoints (PCK) [56]. The predicted keypoints are considered to be correct if they lie within $\alpha \cdot \max(h, w)$ pixels from the ground-truth keypoints for $\alpha \in [0, 1]$, where $h$ and $w$ are the height and width of either an image ($\alpha_{img}$) or an object bounding box ($\alpha_{bbox}$).

Experimental Configuration. For the feature extractor, we use ResNet-101 [15] pre-trained on ImageNet with a single feature at stride 16. Learnable parameters are randomly initialized. For our base model, we set Efficient SCE kernel size $K = 7$ and $d_g = 2048$ for SPair-71k; $K = 13$ and $d_g = 1024$ for PF-PASCAL, resp. We upsample the correlation map to stride 4 for high-resolution loss. For label mask dilation, dilation kernel size $k = 7$ is set for both SPair-71k and PF-PASCAL by validation search. For dynamic label selection, we set $R(T)$ linearly increases from the ratio of 20% to 90% in a duration of 10 epochs for both SPair-71k and PF-PASCAL. $\lambda$ is 10.0 for weighting pseudo-loss. We strictly follow previous work for data augmentation [6] (e.g., color jittering) except that [6] uses ground truth box for random crop while we do not. An AdamW
Table 2. Comparison with SOTA methods on PF-PASCAL [10]. Numbers in bold indicate the best performance and underlined ones are the second best. † means ground truth bbox used.

| Sup. Methods | PCK@α_{img} | α=0.05 | α=0.10 | α=0.15 | α=0.1 |
|--------------|-------------|---------|---------|---------|--------|
| none         | PF-LOM [10] | 31.4    | 62.5    | 79.5    | 45.0   |
| self         | CNNGeoResNet-101 [14] | 41.0    | 69.5    | 89.4    | 68.0   |
| weak         | WeakAlignResNet-101 [35] | 49.0    | 74.8    | 84.0    | 72.0   |
|              | NC-NetResNet-101 [46] | 54.3    | 78.9    | 86.0    | 70.0   |
|              | DCCNetResNet-101 [22] | 55.6    | 82.3    | 90.5    | -      |
|              | GSFResNet-101 [25] | 62.8    | 84.5    | 93.7    | -      |
| trn-none     | HPFResNet-101 [40] | 60.1    | 84.8    | 92.7    | 78.5   |
| val-strong   | SCOTResNet-101 [38] | 63.1    | 85.4    | 92.7    | -      |
| strong       | SCNetVGG-16 [12] | 36.2    | 72.2    | 82.0    | 48.2   |
|              | ANCNetResNet-101 [36] | -       | 86.1    | -       | -      |
|              | DHPFResNet-101 [42] | 75.7    | 90.7    | 95.0    | 87.8   |
|              | PMDResNet-101 [36] | -       | 90.7    | -       | -      |
|              | MMNetResNet-101 [61] | 77.6    | 89.1    | 94.3    | -      |
|              | CHMResNet-101 [39] | 80.1    | 91.6    | -       | -      |
|              | CATsResNet-101 [6] | 75.4    | 92.6    | 96.4    | 89.2   |
|              | PMNCResNet-101 [31] | 82.4    | 90.6    | -       | -      |
| Ours (ST)    | ResNet-101 | 81.4    | 92.9    | 96.1    | 90.5   |
| Ours (MT)    | ResNet-101 | 81.5    | 93.3    | 96.6    | 91.2   |

5.2 Comparison with State-of-the-art Methods

SPair-71k. We compare our method with the most recent work [40,38,42,61,31,6] on SPair-71k in Table 1. Our two variant settings (ST and MT) both achieve an overall SOTA results, with our method (MT) achieving an overall PCK (α_{img} = 0.1) of 55.3%, outperforming the previous SOTA [31] by a large margin (4.9%). Note that our method does not involve any parameterized correlation refinement compared with [31], clearly illustrating the power of the proposed pipeline. Fig. 4 shows qualitative results on SPair-71k. We observe that our method is robust to diverse variations in scale and viewpoint thanks to our enriched training signals.

PF-PASCAL. Our results on PF-PASCAL are summarized in Table 2. Our method outperforms the previous state-of-the-art [31,6] on almost all thresh-
olds even if the performance on PF-PASCAL is near saturated, reaching a new SOTA of 93.3% PCK ($\alpha = 0.1$). Note that even if we did not use sophisticated parameterized correlation map refinement as in PMNC [31], we can still achieve comparable PCK at $\alpha = 0.05$.

**PF-WILLOW.** We test on PF-WILLOW [9] using our model trained on PF-PASCAL [10] to verify dataset generalization ability of our method. As shown in Table 3, our method (MT) outperforms the prior SOTA [39,6] in $\alpha = 0.05$, 0.1 by 1.4% and 0.6%, resp, indicating superior dataset generalization ability of our learning method. Note that our method (MT) are 0.5% behind at $\alpha = 0.15$ compared with [6], we argue that CATs [6] used ground truth bounding box during training while we did not.

### 5.3 Ablation Study

In this section, we conduct ablation studies to verify the effectiveness of each individual module of the proposed model. We train all the variants on the training split of SPair-71k [41] and report PCK ($\alpha_{bbox} = 0.1$) on the test split. Each ablation experiment is conducted under the same experimental setting for a fair comparison.
Table 3. Comparison with SOTA methods on PF-WILLOW [9]. Numbers in bold indicate the best performance and underlined ones are the second best. † means ground truth bbox used.

| Sup.  | Methods                      | PCK\(\alpha_{bbox}\) |
|-------|------------------------------|-----------------------|
|       |                              | \(\alpha = 0.05\) | \(\alpha = 0.10\) | \(\alpha = 0.15\) |
| none  | PF-LOM [10]                  | 28.4                  | 56.8                | 68.2                |
| self  | CNNGeoResNet-101 [44]        | 36.9                  | 69.2                | 77.8                |
| weak  | WeakAlignResNet-101 [45]     | 37.0                  | 70.2                | 79.9                |
|       | NC-NetResNet-101 [46]        | 44.0                  | 72.7                | 85.4                |
|       | DCCNetResNet-101 [22]        | 43.6                  | 73.8                | 86.5                |
|       | GSFResNet-101 [25]           | 47.0                  | 75.8                | 88.9                |
| trn-none | HPFResNet-101 [40]         | 45.9                  | 74.4                | 85.6                |
| val-strong | SCOTResNet-101 [38]     | 47.8                  | 76.0                | 87.1                |
| strong | SCNetVGG-16 [12]             | 38.6                  | 70.4                | 85.3                |
|       | DHPFResNet-101 [42]          | 49.5                  | 77.6                | 89.1                |
|       | PMDResNet-101 [36]           | -                     | 75.6                | -                   |
|       | CHMResNet-101 [39]           | 52.7                  | -                   | 79.4                |
|       | CATs1 ResNet-101 [6]         | 50.3                  | 79.2                | 90.3                |
| Ours (ST) | ResNet-101                | 53.5                  | 79.4                | 89.5                |
| Ours (MT) | ResNet-101                | 54.1                  | 80.0                | 89.8                |

Effect of individual modules. Table 4 summarizes the ablation results of each individual module. First, we note that applying the proposed Efficient-SCE (ID A1) yields significant gain over the baseline (ID A0), showing the effectiveness of the proposed feature enhancement module. Second, enforcing high-resolution loss improves to a remarkable 49.8% after finetuning (ID A3). Our proposed network achieves competitive results without any Conv4D or transformer modules for correlation map refinement. Third, densifying labels combined with our two denoising techniques achieves 5.5% boost further and promotes the performance to 55.3%, showing the effectiveness of our proposed learning strategy. In contrast, teacher-student learning alone without any denoising provides little boost as the dense pseudo-labels might be too noisy (ID A4).

Single offline Teacher vs. Mutual online Teacher. Table 5 shows the comparison between our proposed two variants of teacher-student learning. Both settings have greatly surpassed the performance of the base network (ID A3), showing the effectiveness of our proposed label densification strategy. We note that the mutual online teacher setting is 2.9% higher than the single offline teacher setting. The reason could be that performance is bounded by the fixed teacher model while the mutual online teacher setting could improve each other over the training process.
Table 4. Effects of each component on SPair-71K [41] test split. HRLoss refers to high-resolution loss, FT refers to finetuning the backbone, Teacher-Student here refers to the variant with mutual online teacher.

| Model ID | Efficient-SCE | HRLoss | Finetune | Teacher-Student | Label Denoise | PCK |
|----------|----------------|--------|----------|-----------------|--------------|-----|
| A0       | -              | -      | -        | -               |              | 14.7|
| A1       | ✓              | -      | -        | -               |              | 33.4|
| A2       | ✓              | ✓      | -        | -               |              | 40.6|
| A3       | ✓              | ✓      | ✓        | -               |              | 49.8|
| A4       | ✓              | ✓      | ✓        | ✓               |              | 49.7|
| A5       | ✓              | ✓      | ✓        | ✓               | ✓            | 51.5|
| A6       | ✓              | ✓      | ✓        | ✓               | ✓            | 55.3|

Table 5. Comparing single offline teacher and mutual online teacher setting on SPair-71K [41] test split.

| Variant Setting          | PCK |
|--------------------------|-----|
| none                     | 49.8|
| single offline teacher   | 52.4|
| mutual online teacher    | 55.3|

Table 6. Effects of kernel size for label mask dilation on SPair-71K [41] test split.

| Dilation Kernel Size | PCK |
|----------------------|-----|
| none                 | 49.8|
| 3                    | 54.0|
| 7                    | 55.3|
| 15                   | 52.0|

Effects of kernel size for label mask dilation. Table 6 summarizes the results of different kernel size for label mask dilation. When increasing the kernel size, the performance rises first but then drops, with kernel size 7 being the best, which demonstrates the necessity of restricting pseudo-labels in a meaningful local neighborhood.

6 Conclusion

In this work, we propose a novel teacher-student learning paradigm in order to address the challenge of label sparsity for semantic correspondence task. In our teacher-student paradigm, we generate dense pseudo-labels by the teacher networks which are trained with sparse annotations. To improve quality of pseudo-labels, we develop two novel techniques to denoise pseudo-labels. Specifically, we first dilate the sparse label masks derived from the sparse keypoint annotations to suppress background pseudo-labels. A dynamic label selection strategy is then introduced to further filter noisy labels. We investigate two variants of the proposed learning paradigm, a single offline teacher setting, and a mutual online teacher setting. Our method achieves state-of-the-art performances on three standard datasets. The effectiveness of our method provides new insight into the problem, and is one step closer towards a more realistic application of semantic correspondence.
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