Flux Erosion of Magnetic Clouds by Reconnection With the Sun’s Open Flux

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Abstract Magnetic clouds (MCs) are flux rope magnetic structures forming a subset of solar coronal mass ejections, which have significant space weather impacts. The geoeffectiveness of MCs depends on their properties, which evolve during their interplanetary passage. Based on an analysis of observations spanning two solar cycles, we establish that MCs interacting with the ambient solar wind magnetic field (i.e., heliospheric open flux) lose a substantial amount of their initial magnetic flux via magnetic reconnection, which, in some cases, reduce their geoeffectiveness. We find a linear correlation between the eroded flux of MCs and solar open flux which is consistent with the scenario that MC erosion is mediated via the local heliospheric magnetic field draping around an MC during its interplanetary propagation. The solar open flux is governed by the sunspot cycle. This work therefore uncovers a hitherto unknown pathway for solar cycle modulation of the properties of MCs.

Plain Language Summary Vast eruptions of magnetized plasma from the Sun known as coronal mass ejections (CMEs) are the main contributors to severe space weather conditions. The magnetic properties of CMEs—which determine their geoeffectiveness—evolve during their interplanetary journey. Therefore, it is important to understand the physical processes that govern their evolution. Based on in situ satellite observations, and modeling here, we provide evidence that the magnetic flux of CME associated magnetic clouds erode over their interplanetary journey due to reconnection with the ambient heliospheric open flux. We also demonstrate that this flux erosion impacts the geoeffectiveness of magnetic clouds in some cases. This mechanism establishes a novel connection between the solar cycle variation of the heliospheric open flux and space weather in the vicinity of solar system planets.

1. Introduction

Coronal mass ejections (CMEs) are magnetized plasma structures expelled sporadically from the Sun and travel toward the heliosphere as interplanetary CMEs (ICMEs). If an ICME has a smoothly rotating strong magnetic field and a low proton temperature (Burlaga et al., 1981; Klein & Burlaga, 1982), it is categorized as a magnetic cloud (MC). The twisted flux ropes of MCs (Burlaga, 1988; Goldstein, 1983; Lepping et al., 1990) carry a significant amount of solar magnetic flux and helicity (Pal et al., 2017). While propagating through the interplanetary medium, the presence of a relative motion between an MC and the ambient plasma would result in a draping of the ambient interplanetary magnetic field (IMF) over the MC (Gosling & McComas, 1987). Such draping has been directly observed (e.g., Crooker et al., 1985) as well as modeled (e.g., Alksne & Webster, 1970). If the magnetic field orientation of the MC is opposite to that of the draped IMF, the process of magnetic reconnection (henceforth reconnection) is initiated (McComas et al., 1988). Due to this reconnection, a part of the MC’s magnetic flux is eroded away and an asymmetry is generated in its azimuthal magnetic flux that accumulates along the spacecraft trajectory. This fact has been established by observations (Dasso et al., 2006, 2007; Möstl et al., 2008; Ruffenach et al., 2012, 2015) as well as by using global MHD simulations (Schmidt & Cargill, 2003; Taubenschuss et al., 2010). Lavraud et al. (2014) showed that erosion of an MC’s magnetic flux may reduce its geoeffectiveness by a significant amount. Figure 1 shows an idealized schematic diagram of the draping of a purely radial ambient IMF about a fast moving MC and the MC’s cross section in a plane perpendicular to the ecliptic plane. The imbalance in the MC’s accumulated azimuthal flux arises due to the reconnection at the MC’s front.

An approximate understanding of the erosion of the magnetic flux of MCs due to reconnection with the IMF can be obtained with recourse to the Sweet-Parker model (Parker, 1957; Sweet, 1958). In the diffusion
region (a small-scale region surrounding the reconnection site) Cassak and Shay (2007) showed that the reconnection rate scales as $E_{\text{rec}} \sim V_1B_1 \sim V_2B_2$, where $V$ and $B$ are the plasma flow speed and magnetic field intensity, respectively, and the subscripts “1” and “2” refer to either side of the inflow region. For steady state reconnection $E_{\text{rec}}$ is uniform at the reconnection region, where $E_{\text{rec}}$ defines the rate of magnetic flux that is transferred from the inflow to the dissipation region (Nakamura et al., 2018). This transferred magnetic flux determines the amount of flux erosion ($F_{\text{er}}$) and one expects that $F_{\text{er}}$ would scale linearly with the background IMF field strength (Cassak & Shay, 2007).

The local Alfvén speed ($V_A$) in the plasma near the reconnection site governs the reconnection rate (Birn et al., 2001; Cassak & Shay, 2007; Parker, 1973). As $V_A$ decreases with the increasing heliospheric distance, the reconnection rate is expected to be higher closer to the Sun and in the inner heliosphere (e.g., Gosling & Szabo, 2008). Dasso et al. (2007) found an extended coherent magnetic region just behind an MC and interpreted that this region is formed due to the reconnection process, which started $\approx 54$ hr before the MC was observed. Lavraud et al. (2014) suggested that about 47% to 67% of the MC erosion is expected to occur within the orbit of Mercury ($\approx 0.39$ AU from the Sun). Ruffenach et al. (2015) found no correlation between the eroded amount of magnetic flux and the ambient solar wind properties observed in situ at 1 AU. The lack of correlation suggests that most of the reconnection is expected to occur during the MC’s passage through the inner heliosphere and not at 1 AU.

Large-scale open magnetic field originating from the solar corona extends out into the heliosphere and shapes the IMF. Utilizing the observed solar photospheric magnetic field information as boundary condition the heliospheric magnetic field can be reconstructed following the simplest assumption that the solar corona is current-free (Schatten et al., 1969). This approach is known as Potential Field Source Surface extrapolation (PFSS). In the outer radial boundary of the PFSS model the field lines are constrained to be radial, which is consistent with the observations of the coronal hole foot points (Wang et al., 1996). The open magnetic flux ($\phi_{\text{open}}$) derived using the Sun’s open magnetic field lines can be used to estimate the radial IMF intensity at any heliocentric distance from the Sun as the Ulysses spacecraft measurements show a latitudinal and longitudinal uniformity of the IMF’s radial component (Balogh et al., 1995; Erdős & Balogh, 2014; Smith & Balogh, 2008). Therefore, the radial magnetic field intensity ($|B_r|$) can be expressed as $|B_r| = |\phi_{\text{open}}|/4\pi r^2$ at a heliocentric distance $r$ ($r \gg R_\odot$). If $\theta_{\text{HG}}$ and $\phi_{\text{HG}}$ are the heliographic latitude and longitude, respectively, then the open magnetic flux can be derived by integrating $|B_r(R_{\text{sv}},\theta_{\text{HG}},\phi_{\text{HG}})|$ over the surface of a sphere.
concentric to the Sun with radius $R_{ss}$, known as source surface. Using $\phi_{\text{open}}$, several studies have estimated $B_r$ at $r = 1$ AU and compared it with the in situ near-Earth radial IMF intensity. The studies found a good correspondence between the estimated and observed values (Wang & Sheeley, 2015; Wang & Sheeley, 1988, 1995; Wang et al., 2000; Yeates et al., 2010).

The present study aims to establish a connection between the MC's eroded magnetic flux and the IMF intensity. For achieving this, we explore the relationship between annual averages of MC's eroded flux and the $\phi_{\text{open}}$ over two solar cycles. Also, we present a statistical analysis to investigate the geomagnetic effectiveness of eroded MCs. We describe the data and their sources in section 2 and present our analysis methodology in section 3. Results are presented in section 4 followed by discussion and conclusions in sections 5 and 6, respectively.

2. Instrumentation and Overview of Data

We use 64 s average Level 2 (verified) data of merged IMF and solar wind parameters (https://www.srl.caltech.edu/ACE/ASC/level2/lvl2DATA&urluscore;MAG-SWEPAM.html) from the Advanced Composition Explorer (Stone et al., 1998) spacecraft’s Solar wind Electron, Proton and Alpha Monitor (McComas et al., 1998), and Magnetic Field Experiment (Smith et al., 1998) instruments. The selected data is in Geocentric Solar Ecliptic (GSE) coordinate system and available since the year 1998. In GSE coordinate system $\hat{x}_{\text{GSE}}$ points toward the Sun, $\hat{z}_{\text{GSE}}$ points toward the North Pole (of the ecliptic) and $\hat{y}_{\text{GSE}}$ completes the right-handed system. To obtain the geomagnetic response of MC, we use the geomagnetic activity index ($D_{st}$) available at the World Data Center, Kyoto (https://wdc.kugi.kyoto-u.ac.jp/dstdir/index.html) in a temporal resolution of 1 hr.

We obtain the radial magnetic field data from synoptic magnetograms (https://hmi.stanford.edu/data/synoptic.html) collected by the Michelson Doppler Imager (MDI) (Scherrer et al., 1995) onboard the Solar and Heliospheric Observatory (Domingo et al., 1995) and the Helioseismic and Magnetic Imager (HMI) (Scherrer et al., 2012) onboard the Solar Dynamics Observatory (Pesnell et al., 2012). The data from MDI and HMI is collected for a period of 1998 to April 2010 and May 2010–2018, respectively. We utilize the radial magnetic field data to extrapolate the coronal magnetic field till the source surface at $r = R_{ss} = 2.5R_\odot$ using a global PFSS extrapolation model.

2.1. MC Events and Criteria For Selection

In general, MCs are identified following the criteria defined by Burlaga et al. (1981), which are (1) throughout an MC interval the magnetic field intensity enhances (compared to the ambient solar wind), (2) smooth rotation in both $B_{y_{\text{GSE}}}$ and $B_{z_{\text{GSE}}}$ components exists, (3) the proton temperature falls below the expected solar wind temperature (Lopez & Freeman, 1986), and (4) the plasma $\beta$ parameter is less than 1. For solar cycle 23 (1998–2007) we consider 37 MCs from a list of 109 MCs selected by Ruffenach et al. (2015). The study categorized the MCs as Q1 (both the front and rear boundaries of MCs are well determined), Q2 (any one of the two boundaries is identified without ambiguity), and Q3 (both the boundaries are difficult to identify). Of them, we select only Q1 and Q2 type MCs for our study as the fitting of flux ropes to the MCs is impacted by incorrect boundary selection. The events during 2008-2014 are obtained from the MC list published by Gopalswamy et al. (2015), and the events of 2015–2018 are selected from the Richardson and Cane (2010) ICME catalogue (https://www.srl.caltech.edu/ACE/ASC/DATA/level3/icmetable2.htm) after manually identifying each of their boundaries. Thus, we select a total number of 35 events during Solar Cycle 24. Note that each of the events selected here is consistent with Burlaga et al.’s (1981) definition of MCs. For none of the events, the spacecraft crosses the MC flux ropes parallel to the legs. This is because those cases lead an azimuthal flux asymmetry which may be misinterpreted as a result of erosion (Ruffenach et al., 2015). Also, there exist uncertainties in fitting parameters (e.g., Marubashi & Lepping, 2007; Lepping et al., 2003), while those MCs are fit with the cylindrical flux rope model. Janvier et al. (2013) introduced a location angle ($\lambda$) measured from the plane ($\hat{y}_{\text{GSE}}, \hat{z}_{\text{GSE}}$) toward the MC axis. It is a proxy for the spacecraft crossing distance from the MC nose. The $\lambda$ evolves monotonically along the MC flux rope with $\lambda = -90^\circ$ in one leg, $\lambda = 0^\circ$ at its nose, and $\lambda = 90^\circ$ in the other leg. Ruffenach et al. (2015) estimated that errors in the azimuthal flux imbalance is less than 10% if $\lambda$ holds a value between $\pm 45^\circ$. Thus, we study only those MCs that cross the spacecraft trajectory sufficiently close to their apex by selecting $\lambda < |45^\circ|$. 

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Figure 2. Plots depicting $B_{\text{cloud}}$ (blue) and $\phi_y/L$ (red) variations of two MCs during their passage past the spacecraft. The black and green vertical dash-dotted lines represent $l_{\text{center}}$ and the zero crossing of $\phi_y/L$ curves, respectively.

(a) For an event where the flux erosion is at the MC front. Here $\phi_{az} = 3.02 \times 10^{21}$ Mx/AU and eroded flux = $6.98 \times 10^{20}$ Mx/AU. (b) For an event where the flux erosion is at MC rear. Here $\phi_{az} = 6.06 \times 10^{20}$ Mx/AU and eroded flux = $2.04 \times 10^{20}$ Mx/AU.

3. Analysis Methodology

Several case studies (Dasso et al., 2006, 2007) show the presence of unbalanced azimuthal magnetic flux in MCs although MCs maintain a classical characteristic. Since the outer part of an MC is mainly affected by reconnection and the azimuthal flux is much greater than the axial flux in there (Ruffenach et al., 2015), the asymmetry is mainly observed in the MC’s azimuthal magnetic flux. To estimate this asymmetry, we employ the “direct method” developed by Dasso et al. (2006).

3.1. Measurement of MC’s Eroded Magnetic Flux

The direct method uses the principle of magnetic flux conservation ($\nabla \cdot B = 0$) across the plane formed by the spacecraft trajectory and MC axis to determine and analyse the MC’s accumulated azimuthal magnetic flux. The MC axis orientation is defined by a latitude angle $\theta$ (the angle between MC’s axis and the ecliptic plane) varying from $-90^\circ$ to $90^\circ$ and a longitude angle $\phi$ (the angle between the projection of MC’s axis on the ecliptic plane and the Earth-Sun direction) varying from $0^\circ$ to $360^\circ$. Using $\theta$ and $\phi$, we rotate the observed MC from GSE to the local MC coordinate defined by Dasso et al. (2006) and derive $B_{\text{cloud}}$ and $V_{\text{cloud}}$ from $B_{\text{GSE}}$ and $V_{\text{GSE}}$. To obtain $\theta$ and $\phi$, we use a constant-$\alpha$ force-free flux rope model (Burlaga, 1988; Marubashi, 1986) to least squares fit the observed MCs. The model follows the equation $V \times B = \alpha B$, where $\alpha$ is a constant.
where $\alpha$ is a constant and allows self-similar expansion of an MC. The Lundquist’s solution to the equation (Lepping et al., 1990) provides the modeled magnetic field vectors in the cylindrical coordinate system. After performing a series of iterations through proper adjustment of model parameters based on minimizing the difference between modeled and observed magnetic field vectors, a final set of best fit parameters including $\theta$ and $\phi$ are ascertained (e.g., Marubashi & Lepping, 2007; Ruffenach et al., 2012).

If $\theta$, $\phi$, and the time of MC front ($t_{\text{front}}$) and rear boundaries ($t_{\text{rear}}$) are known, the accumulated azimuthal magnetic flux per unit length ($\frac{\phi_{\text{az}}(t_{1}, t_{2})}{L}$) can be measured using

$$\frac{\phi_{\text{az}}(t_{1}, t_{2})}{L} = \int_{t_{1}}^{t_{2}} B_{z, \text{cloud}}(t)V_{x, \text{cloud}} dt,$$

where $L$ is the total length of the MC axis till 1 AU, $B_{z, \text{cloud}}$, and $V_{x, \text{cloud}}$ are the MC's magnetic field and velocity components computed in the local cloud coordinate system, respectively. The times $t_{1}$ and $t_{2}$ represent generic times defining the boundaries of the integral. The normalized perpendicular distance between spacecraft trajectory and MC axis is called the impact parameter ($y_{0}$). The accumulated azimuthal flux is more precisely estimated when $y_{0}$ is low. In Figure 2 we plot the time evolution of $B_{z, \text{cloud}}$ (blue curve) along with $\phi_{\text{az}} / L$ (red curve) of two MCs during their passage through the spacecraft. Figure 2a shows an MC that is eroded at the front edge. The parameter $\phi_{\text{az}} / L$ is calculated considering $t_{1} = t_{\text{front}}$ and $t_{2} = t_{\text{rear}}$. Due to erosion its accumulated azimuthal flux shows an excess at its rear. The total azimuthal flux per unit length ($\phi_{\text{az}}$) that was originally present in that MC (before erosion) is estimated by the unsigned value of $\phi_{\text{az}}(t_{\text{center}}, t_{\text{rear}}) / L$. Here $t_{\text{center}}$ (shown in dashed-dotted black vertical lines in Figures 2a and 2b) is the time when $B_{z, \text{cloud}}$ changes its sign and results in a maximum value of unsigned $\phi_{\text{az}} / L$. The time $t_{\text{center}}$ is the time when closest approach of the spacecraft to the MC axis is achieved. The eroded azimuthal flux (per unit length) of the MC is represented by the absolute value of $\phi_{\text{az}} / L$ at $t_{\text{rear}}$. The second MC (Figure 2b) is eroded at its rear and shows a flux imbalance at its front. Here $\phi_{\text{az}} / L$ is calculated considering $t_{1} = t_{\text{rear}}$ and $t_{2} = t_{\text{front}}$. For this case $\phi_{\text{az}}$ is estimated by the unsigned value of $\phi_{\text{az}}(t_{\text{center}}, t_{\text{front}}) / L$. The eroded flux of the MC is defined by the absolute value of $\phi_{\text{az}} / L$ at $t_{\text{front}}$. We next define $\phi_{\text{erod}}$ as the eroded flux normalized to $\phi_{\text{az}}$. The dash-dotted green vertical lines show the estimated rear (Figure 2a) and front (Figure 2b) boundaries of the remaining flux rope when it is observed in situ.

3.2. Estimation of the Sun’s Open Flux
An estimate of the Sun’s open flux is traditionally made based on potential field extrapolation of the Sun’s coronal field (satisfying $\nabla \times \mathbf{B} = 0$; Schatten et al., 1969). Following van Ballegooijen et al. (2000) and using a module developed by Yeates (2018), we extrapolate the coronal magnetic field utilizing solar surface synoptic maps from MDI and HMI as the lower boundary condition. The unsigned open flux ($|\phi_{\text{open}}|$) is estimated at $R_{\odot} = 2.5R_{\odot}$. We obtain a strong positive correlation (with linear correlation coefficient, $r_{p} = 0.89$ at 99.99% confidence level) between the yearly averaged IMF intensity observed in situ at 1 AU and $|\phi_{\text{open}}|$. Therefore, $|\phi_{\text{open}}|$ can be used as a proxy of the IMF intensity.

4. Analysis and Results

By applying the direct method to all the selected MCs, we derive $\phi_{\text{az}}$, $\phi_{\text{erod}}$, and the position of the flux imbalance (front or back) for each of the MCs. In Figure 3a we demonstrate the effect of MC’s erosion on its geoeffectiveness by plotting MC’s remaining azimuthal flux ($\phi_{\text{az}}$—eroded flux) versus its geomagnetic response (quantified by $\Delta$St$_{\text{m}}$—the minimum value of $\Delta$St during an MC’s passage). The correlation between the remaining flux and $\Delta$St$_{\text{m}}$ ($r_{p} = -0.7$ at 99.99% confidence) is slightly lower than the correlation between total flux and $\Delta$St$_{\text{m}}$ ($r_{p} = -0.76$ at 99.99% confidence) if all events are considered. However, it is to be noted that the impact of MC’s azimuthal flux erosion on its geomagnetic response is expected only if $B_{z, \text{GSE}}$ has a negative value at the reconnection site and the MC's azimuthal field component corresponds to $B_{z, \text{GSE}}$ (i.e., $\theta, \lambda \sim 0^{\circ}$) near the Earth (i.e., at 1 AU). Our sample has nine MCs (depicted by red dots in Figure 3a), which have negative $B_{z, \text{GSE}}$ at their reconnection sites and $|\theta|, |\lambda| \leq 30^{\circ}$ (i.e., close to the above conditions, while still providing reasonable sample size). For these events the correlation between the remaining flux of MCs and $\Delta$St$_{\text{m}}$ is higher ($r_{p} = -0.95$ at 99.99% confidence) compared to that between $\phi_{\text{az}}$ and $\Delta$St$_{\text{m}}$ ($r_{p} = -0.88$ at 99.99% confidence). This reveals the impact of flux erosion on the geoeffectiveness of MCs.

We notice that out of 72, 40 MCs show the flux imbalance at rear with an average value of $\phi_{\text{erod}} \sim 0.26$ and 32 MCs show flux imbalance at front with an average $\phi_{\text{erod}} \sim 0.23$. The average eroded flux irrespective of
Figure 3. (a) Scatter plot between the remaining flux of MCs and their geoeffectiveness as quantified by the minimum Dst index ($D_{st,min}$). Least squares fit considering all events (red and black dots) and the correlation are shown in black. For a subset of events (red dots only) as described in the text, the corresponding least squares fit and correlation are depicted in red. (b) $\overline{\phi_{erod}}$ and $\overline{|\phi_{open}|}$ plotted against each year for solar cycle 23 and 24 in continuous red and dashed black curves, respectively. Vertical lines in corresponding colors represent the error bars for $\overline{\phi_{erod}}$ and $\overline{|\phi_{open}|}$. (c) Scatter plot of $\overline{|\phi_{open}|}$ versus $\overline{\phi_{erod}}$. The over plotted blue solid line shows the least squares fit to the data points. The correlation is mentioned in blue.
the erosion position during Solar Cycles 23 and 24 are found to be 0.276 and 0.22, respectively. Our result matches well with the value of normalized average eroded flux found by Ruffenach et al. (2015) for the events during Solar Cycle 23. MCs showing flux imbalance at the front or rear boundaries are named as MCF and MCR, respectively. In Table 1, we show the number of total MCs (Column 2), MC$_R$ (Column 3), MC$_F$ (Column 4), annual averages of $\phi_{erod}$ (Column 5), and unsigned $\phi_{open}$ (Column 6) with their standard deviations corresponding to each year mentioned in Column 1.

### Table 1

| Year | $N_{MC}$ | MC$_R$ | MC$_F$ | $\bar{\phi}_{erod}$ | $\bar{\phi}_{open}$ $(\times 10^{22} \text{Mx})$ |
|------|----------|--------|--------|----------------------|---------------------------------|
| 1998 | 5        | 2      | 3      | 0.24 ± 0.13          | 2.18 ± 0.21                     |
| 1999 | 3        | 2      | 1      | 0.28 ± 0.06          | 4.12 ± 0.45                     |
| 2000 | 5        | 4      | 1      | 0.47 ± 0.11          | 5.11 ± 0.25                     |
| 2001 | 4        | 2      | 2      | 0.29 ± 0.13          | 4.43 ± 0.22                     |
| 2002 | 3        | 3      | 0      | 0.42 ± 0.14          | 7.08 ± 0.28                     |
| 2003 | 2        | 0      | 2      | 0.16 ± 0.05          | 6.24 ± 0.29                     |
| 2004 | 5        | 4      | 1      | 0.17 ± 0.10          | 3.17 ± 0.21                     |
| 2005 | 3        | 1      | 2      | 0.24 ± 0.06          | 2.76 ± 0.11                     |
| 2006 | 3        | 3      | 0      | 0.24 ± 0.09          | 1.76 ± 0.16                     |
| 2007 | 2        | 0      | 2      | 0.16 ± 0.06          | 1.06 ± 0.05                     |
| 2008 | 2        | 2      | 0      | 0.12 ± 0.12          | 1.01 ± 0.08                     |
| 2009 | 4        | 1      | 3      | 0.19 ± 0.05          | 0.61 ± 0.04                     |
| 2010 | 3        | 1      | 2      | 0.11 ± 0.08          | 1.17 ± 0.06                     |
| 2011 | 1        | 1      | 0      | 0.22 ± 0.00          | 1.60 ± 0.10                     |
| 2012 | 9        | 4      | 5      | 0.20 ± 0.05          | 1.74 ± 0.09                     |
| 2013 | 10       | 6      | 4      | 0.28 ± 0.08          | 2.15 ± 0.17                     |
| 2014 | 3        | 0      | 3      | 0.31 ± 0.17          | 3.06 ± 0.41                     |
| 2015 | 1        | 1      | 0      | 0.15 ± 0.00          | 3.05 ± 0.16                     |
| 2016 | 2        | 2      | 0      | 0.11 ± 0.10          | 2.20 ± 0.10                     |
| 2017$^a$ | 0      | 0      | 0      | —                   | 1.23 ± 0.03                     |
| 2018 | 2        | 1      | 1      | 0.27 ± 0.23          | 0.92 ± 0.05                     |

$^a$None of the observed MCs follow our selection criteria.

4.1. Comparison Between the Sun’s Unsigned Open Flux and MC Flux Erosion

The erosion of magnetic flux in an MC depends on the rate of reconnection between the magnetic field of the MC and IMF. As it is stated before that the reconnection rate scales with the IMF intensity, a correlation is expected between $\phi_{erod}$ and the prevailing IMF strength whose proxy is the unsigned $\phi_{open}$. We define the yearly average of the normalized eroded azimuthal flux ($\bar{\phi}_{erod}$) by averaging over $\phi_{erod}$ with the total number of events ($N_{MC}$) in each year. In Figure 3b, we plot $\bar{\phi}_{erod}$ and the yearly average of unsigned $\phi_{open}$ ($|\bar{\phi}_{open}|$) in solid red and dashed black curves, respectively, along with error bars over the period encompassing Solar Cycles 23 and 24. The error bars are calculated by estimating $\sigma / \sqrt{N_{MC}}$, where $\sigma$ is the standard deviation and $N_{MC}$ represents number of MC events for the eroded flux and number of PFSS extrapolations for the calculation of the open flux in each year. A correlation study is performed between $\bar{\phi}_{erod}$ and $|\bar{\phi}_{open}|$. We obtain a Pearson correlation coefficient ($r_p$) of 0.56 and a Spearman's rank correlation coefficient ($r_s$) of 0.44, at 99% and 95% confidence levels, respectively. To confirm our result, we compute $r_p$ including the parameters' error bar information and find the value of $r_p$ as 0.51 ± 0.03 at 98% confidence level. In Figure 3c, we show a scatter plot between $\bar{\phi}_{erod}$ and $|\bar{\phi}_{open}|$. The observed correspondence between the eroded flux and the Sun’s open flux indicates an underlying linear relationship between the reconnection rate and the IMF intensity. To relate these two parameters, we perform a least squares fit to $|\bar{\phi}_{open}|$ versus $\bar{\phi}_{erod}$, which gives...
the following equation

\[ \phi_{\text{erod}} = 0.06|\phi_{\text{open}}| + 0.06, \]  

where \( |\phi_{\text{open}}| \) is in units of \( 10^{22} \text{ Mx} \). The solid blue line over plotted on the scatter plot represents the least squares fitting.

5. Discussion

To establish a correspondence between MC’s eroded flux and the IMF intensity, we study the dependency of the MC’s eroded flux on the Sun’s open flux over two solar cycles. We find that about 44% of the total MCs studied here shows an imbalance at their rear boundaries. A numerical simulation of reconnection between an MC and solar wind performed by Schmidt and Cargill (2003) shows an enhancement in reconnection with the increasing relative speed of the MC compared to the solar wind. If an MC is followed and compressed by a fast solar wind, reconnection may occur at the MC’s rear boundary. Such high-speed solar wind primarily originates from polar coronal holes and may extend toward low latitudes (Fenrich & Luhmann, 1998). Also, MCs can be compressed by corotating interaction regions whose formation is related to the presence of coronal holes (Rouillard et al., 2010).

In our study we obtain the orientation of an MC axis by fitting the observed MC using a force-free cylindrical flux rope model. The model is impacted by several factors, such as, incorrect boundary selection (Lepping et al., 2003), non-circular MC cross section (Savani et al., 2011a, 2011b) and high impact parameter values (Démoïlin et al., 2013; Riley et al., 2004). Ruffenach et al. (2015) showed that the flux rope fitting method has a tendency of deriving a consistently lower value of eroded flux because the model is based on axisymmetric geometry. Also, a high impact parameter lowers the total azimuthal magnetic flux that causes an overestimation of the normalized eroded flux.

The imbalance in MC azimuthal flux accumulated along the spacecraft path may occur due to various other reasons. When a high-speed CME propagates from Sun to Earth it undergoes strong deceleration (Jones et al., 2007). If a cool, dense filament material is located at the base of the CME, the momentum of the filament results in its forward movement through the decelerating CME. Thus, the protruding filament drives flow leading to a sideways transport of the CME’s poloidal field. This can generate an azimuthal flux imbalance in the CME flux rope by the time the CME reaches the Earth. Manchester et al. (2014) explained such flux imbalances through simulation of a three-part structure CME observed on 20 January 2005. In such cases, the eroded magnetic flux amount does not depend on the rate of reconnection between the MC and the IMF. This may also contribute to a lower correlation between the amount of eroded MC flux and \( \phi_{\text{open}} \). Nonetheless, we find the correlation to be significant and the underlying relationship between \( \phi_{\text{erod}} \) and \( \phi_{\text{open}} \) to be linear.

6. Conclusions

We establish a relationship between the azimuthal magnetic flux erosion of MCs and the Sun’s unsigned open flux that regulates the IMF intensity. Utilizing the direct method, we investigate 72 MCs spanning Solar Cycles 23 and 24 to estimate the magnetic flux imbalance and erosion. We find that on average 28% and 22% of the total azimuthal magnetic flux of MCs of Solar Cycles 23 and 24, respectively, are eroded during their propagation through the inner heliosphere. The reconnection causing this erosion may occur on either side of the MC boundaries and peel off an almost similar amount of magnetic flux. We compare the annual averages of solar open flux to the average fraction of the eroded magnetic flux of MCs over the past 21 years (from 1998 to 2018) and find a significant positive correlation with an underlying linear relationship. Since the solar open flux is strongly correlated with the IMF intensity, this is suggestive of the latter’s role in MC flux erosion.

We note that the solar open flux is governed by the emergence and redistribution of active region magnetic fields on the Sun’s surface due to surface flux transport processes—a crucial component of the solar dynamo mechanism (Bhowmik & Nandy, 2018). Given that the solar wind dispersed open flux determines
the ambient heliospheric magnetic field (IMF), the latter's solar cycle modulation provides a novel pathway via which the large-scale solar cycle can govern flux erosion and thus possibly the geoeffectiveness of interplanetary MCs.

References

Alksne, A. V. & Webster, D. L. (1970). Magnetic and electric fields in the magnetosheath. Planetary and Space Science. 18(8), 1203–1212.
Balogh, A., Smith, E. J., Tsurutani, B. T., Southwood, D. J., Forsyth, R. J., & Horbury, T. S. (1995). The heliospheric magnetic field over the south polar region of the Sun. Science, 268, 1007–1010. https://doi.org/10.1126/science.268.5213.1007
Bhowmik, P., & Nandy, D. (2018). Prediction of the strength and timing of sunspot cycle 25 reveal decadal-scale space environmental conditions. Nature Communications, 9, 5209. https://doi.org/10.1038/s41467-018-07690-0
Birn, J., Drake, J. F., Shay, M. A., Rogers, B. N., Denton, R. E., Hesse, M., et al. (2001). Geospace Environmental Modeling (GEM) magnetic reconnection challenge. Journal of Geophysical Research, 106, 3715–3720. https://doi.org/10.1029/1999JA900449
Burlaga, L. F. (1981). Magnetic clouds and force-free fields with constant alpha. Journal of Geophysical Research, 93, 7217–7222. https://doi.org/10.1029/JA093iA07p07217
Burlaga, L. F., Hundhausen, A. J., & Zhao, X.-P. (1981). The coronal and interplanetary current sheet in early 1976. Journal of Geophysical Research, 86, 8893–8899. https://doi.org/10.1029/JA096iA11p08893
Cassak, P. A., & Shay, M. A. (2007). Scaling of asymmetric magnetic reconnection: General theory and collisional simulations. Physics of Plasmas, 14(10), 102114. https://doi.org/10.1063/1.2795630
Crooker, N. U., Luhmann, J. G., Russell, C. T., Smith, E. J., Spreiter, J. R., & Stahara, S. S. (1985). Magnetic field draped against the dayside magnetopause. Journal of Geophysical Research, 90(A4), 3505–3510.
Dasso, S., Mandrini, C. H., Démoulin, P., & Luoni, M. L. (2006). A new model-independent method to compute magnetic helicity in magnetic clouds. Astronomy & Astrophysics, 455, 349–359. https://doi.org/10.1051/0004-6361:20064806
Dasso, S., Nakwacki, M. S., Démoulin, P., & Mandrini, C. H. (2007). Progressive transformation of a flux rope to an ICME. Comparative analysis using the direct and fitted expansion methods. Solar Physics, 244, 115–137. https://doi.org/10.1007/s11207-007-9304-2
Démoulin, P., Dasso, S., & Janvier, M. (2013). Does spacecraft trajectory strongly affect detection of magnetic clouds? Astronomy & Astrophysics, 550, A3. https://doi.org/10.1051/0004-6361/201220535
Domingo, V., Fleck, B., & Poland, A. I. (1995). The SOHO mission: An overview. Astrophysics & Space Science, 228, 563–612. https://doi.org/10.1007/BF00733425
Erdös, G., & Balogh, A. (2014). Magnetic flux density in the heliosphere through several solar cycles. The Astrophysical Journal, 781, 50. https://doi.org/10.1088/0004-637X/781/1/50
Fenrich, F. R., & Luhmann, J. G. (1988). Geomagnetic response to magnetic clouds of different polarity. Geophysical Research Letters, 25, 2999–3002. https://doi.org/10.1029/GL014i004p00355
Goldstein, H. (1983). On the field configuration in magnetic clouds, Geophysical Research Letters, 10(A4), 50.

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Pal, S., Gopalswamy, N., Nandy, D., Akiyama, S., Yashiro, S., Makela, P., & Xie, H. (2017). A Sun-to-Earth analysis of magnetic helicity of the 2013 March 17-18 interplanetary coronal Mass ejection. *The Astrophysical Journal, 851*(2), 123. https://doi.org/10.3847/1538-4357/a9983

Parker, E. N. (1957). Sweet’s mechanism for merging magnetic fields in conducting fluids. *Journal of Geophysical Research, 62*(4), 509–520. https://doi.org/10.1029/JZ062i004p00509

Parker, E. N. (1973). The reconnection rate of magnetic fields. *The Astrophysical Journal, 180*, 247–252.

Pesnell, W. D., Thompson, B. J., & Chamberlin, P. C. (2012). The Solar Dynamics Observatory (SDO). *Solar Physics,* 275, 3–15. https://doi.org/10.1007/s11207-011-9841-3

Richardson, I. G., & Cane, H. V. (2010). Near-Earth interplanetary coronal mass ejections during solar cycle 23 (1996–2009): Catalog and summary of properties. *Solar Physics, 264*(1), 189–237. https://doi.org/10.1007/s11207-010-0956-8

Riley, P., Linker, J. A., Lionello, R., Mikić, Z., Odstrcil, D., Hidalgo, M. A., et al. (2004). Fitting flux ropes to a global MHD solution: A comparison of techniques. *Journal of Atmospheric and Solar-Terrestrial Physics,* 66(15–16), 1321–1331. https://doi.org/10.1016/j.jastp.2004.03.019

Rouillard, A. P., Lavraud, B., Sheehy, N. R., Davies, J. A., Burlaga, L. F., Savani, N. P., et al. (2010). White light and in situ comparison of a forming merged interaction region. *The Astrophysical Journal, 719*, 1385–1392. https://doi.org/10.1088/0004-637X/719/2/1385

Ruffenach, A., Lavraud, B., Farrugia, C. J., Démoïlin, P., Dasso, S., Owens, M. J., et al. (2015). Statistical study of magnetic cloud erosion by magnetic reconnection. *Journal of Geophysical Research: Space Physics,* 120, 43–60. https://doi.org/10.1002/2014JA020628

Ruffenach, A., Lavraud, B., Owens, M. J., Sauvaud, J.-A., Savani, N. P., Rouillard, A. P., et al. (2012). Multispacecraft observation of magnetic cloud erosion by magnetic reconnection during propagation. *Journal of Geophysical Research, 117*, A09101. https://doi.org/10.1029/2012JA017624

Savani, N. P., Owens, M. J., Rouillard, A. P., Forsyth, R. J., Kusano, K., Shiota, D., & Kataoka, R. (2011a). Evolution of coronal mass ejection morphology with increasing heliocentric distance. I. Geometrical analysis. *The Astrophysical Journal, 731*(2), 109. https://doi.org/10.1088/0004-637X/731/2/109

Savani, N. P., Owens, M. J., Rouillard, A. P., Forsyth, R. J., Kusano, K., Shiota, D., et al. (2011b). Evolution of coronal mass ejection morphology with increasing heliocentric distance. II. In situ observations. *The Astrophysical Journal, 732*(2), 117. https://doi.org/10.1088/0004-637X/732/2/117

Schatten, K. H., Wilcox, J. M., & Ness, N. F. (1969). A model of interplanetary and coronal magnetic fields. *Solar Physics,* 6(3), 442–455. https://doi.org/10.1007/BF00146478

Scherrer, P. H., Bogart, R. S., Bush, R. I., Hoeksema, J. T., Kosovichev, A. G., Schou, J., et al. (1995). The solar oscillations investigation—Michelson Doppler imager. *Solar Physics,* 162, 129–188. https://doi.org/10.1007/BF00733429

Scherrer, P. H., Schou, J., Bush, R. I., Kosovichev, A. G., Bogart, R. S., Hoeksema, J. T., et al. (2012). The Helioseismic and Magnetic Imager (HMI) investigation for the Solar Dynamics Observatory (SDO). *Solar Physics,* 275, 207–227. https://doi.org/10.1007/s11207-011-9834-2

Schmidt, J. M., & Cargill, P. J. (2003). Magnetic reconnection between a magnetic cloud and the solar wind magnetic field. *Journal of Geophysical Research, 108*(A1), 1023. https://doi.org/10.1029/2002JA009325

Smith, E. J., & Balogh, A. (2008). Decrease in heliospheric magnetic flux in this solar minimum: Recent Ulysses magnetic field observations. *Geophysical Research Letters, 35*, L22103. https://doi.org/10.1029/2008GL035345

Smith, C. W., L’Heureux, J., Ness, N. F., Acuña, M. H., Burlaga, L. F., & Scheifele, J. (1998). The ACE magnetic fields experiment. *Space Science Reviews,* 86, 613–632. https://doi.org/10.1023/A:1005092216668

Stone, E. C., Frandsen, A. M., Mewaldt, R. A., Christian, E. R., Margolis, D., Ormes, J. F., & Snow, F. (1998). The Advanced Composition Explorer. *Space Science Reviews,* 86, 1–22. https://doi.org/10.1023/A:1005082526237

Sweet, P. A. (1958). 14. The neutral point theory of solar flares. *Symposium - International Astronomical Union,* 6, 123–134. https://doi.org/10.1017/S00771890900023704

Taubenschuss, U., Erkaev, N. V., Biernat, H. K., Farrugia, C. J., Möstl, C., & Amerstorfer, U. V. (2010). The role of magnetic handedness in magnetic cloud propagation. *Annales Geophysicae,* 28(5), 1075–1100. https://doi.org/10.5194/angeo-28-1075-2010

van Ballegooijen, A. A., Priest, E. R., & Mackay, D. H. (2000). Mean field model for the formation of filament channels on the Sun. *The Astrophysical Journal, 539*(2), 983–994. https://doi.org/10.1086/309265

Wang, Y.-M., Hawley, S. H., & Sheeley, N. R. (1996). The magnetic nature of coronal holes. *Science,* 271(5248), 464–469. https://doi.org/10.1126/science.271.5248.464

Wang, Y.-M., Lean, J., & Sheeley, N. (2000). The long-term variation of the Sun’s open magnetic flux. *Geophysical Research Letters,* 27, 505–508. https://doi.org/10.1029/2000GL008454

Wang, Y.-M., & Sheeley, N. R. (1988). The solar origin of long-term variations of the interplanetary magnetic field strength. *Journal of Geophysical Research,* 93, 11,227–11,236.

Wang, Y.-M., & Sheeley, N. R. Jr. (1995). Solar implications of ULYSSES interplanetary field measurements. *The Astrophysical Journal Letters,* 447, L143. https://doi.org/10.1086/309578

Wang, Y.-M., & Sheeley, N. Jr. (2015). Coronal mass ejections and the solar cycle variation of the Sun’s open flux. *The Astrophysical Journal Letters,* 809(2), L24.

Yeates, A. R., Mackay, D. H., van Ballegooijen, A. A., & Constable, J. A. (2010). A nonpotential model for the Sun’s open magnetic flux. *Journal of Geophysical Research,* 115, A09112. https://doi.org/10.1029/2010JA015611

Yeates, A. (2018). anteyeates1983/pfss: First release of pfss code. Retrieved from https://doi.org/10.5281/zenodo.1472183