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We investigate three-dimensional ideal hydrodynamic evolution, with Landau initial conditions, incorporating event-by-event variation with many events and transverse density inhomogeneities. We show that the transition to boost-invariant flow occurs too late for realistic setups, with corrections of $O(20-30\%)$ expected at freezeout for most scenarios. Moreover, the deviation from boost-invariance is correlated with both transverse flow and elliptic flow, with the more highly transversely flowing regions also showing the most violation of boost invariance. Therefore, if longitudinal flow is not fully developed at the early stages of heavy ion collisions, hydrodynamics where boost-invariance holds at mid-rapidity is inadequate to extract transport coefficients of the quark-gluon plasma. We conclude by arguing that developing experimental probes of boost invariance is necessary, and suggest some promising directions in this regard.

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The quantitative modeling of matter produced in high energy heavy ion collisions with relativistic hydrodynamics is now a well-established field, following the widely cited announcement that matter produced at the relativistic heavy ion collider (RHIC), behaves as a “perfect fluid” [1–6]. The evidence for this behavior comes from the successful modeling of RHIC anisotropic flow by boost-invariant hydrodynamics [7–13]. It is now clear that the same fluid-like behavior persists at the LHC [14–16]. It is commonly argued that, given precise enough data on soft physics, chiefly momentum spectra and their azimuthal anisotropy, the transport coefficients of matter created in ultrarelativistic heavy ion collisions can be quantitatively constrained. Several research groups are moving in this direction [17–22].

These models are all based on the reduction, either exact or approximate, of the problem to a two-dimensional system [25], based on the symmetry of boost-invariance. Essentially, the system at mid-rapidity is assumed to act or approximate, of the problem to a two-dimensional moving in this direction [17–22].

or, equivalently not on $t, z$ separately, but just on

$$\tau = \sqrt{t^2 - z^2}$$

(evolved from an initial time $\tau_0$) and transverse degrees of freedom. An initial condition that respects Eq. (1) but not Eq. (2) will slowly degrade the constraints of Eq. (1), as shown in [24–26]. 2+1 dimensional codes typically assume both Eq. (1) and Eq. (2). 3+1 dimensional codes can relax either of these assumptions but will yield results at mid-rapidity approximately identical to Eq. (1) and Eq. (2), if boost-invariance is assumed as an initial condition.

Initially, a different model has originally been advocated as the obvious initial state for the hydrodynamic evolution of the fluid: Landau hydrodynamics [27–30]. In this picture, the energy that forms the bulk of the expanding fireball “stops” at midrapidity at time zero (in the collider frame). The initial distribution of matter is therefore a “pancake”, of thickness $2\Delta$ related to the boosted charge radius $R$ of the nuclei with nucleon mass $m_N$ at center of mass energy of $\sqrt{s_{NN}}$ where

$$\Delta \rightarrow \Delta_{\text{im}} \simeq \frac{R}{\gamma} = \frac{Rm_N}{(\sqrt{s_{NN}}/2)}.$$  

In a more general implementation, $\Delta$ need not be defined by Eq. (4) and can be a free parameter, reflecting the spread in configuration space of low $x$ gluons. The initial Landau condition is defined by the assumption that the initial “pancake” has no existing longitudinal flow at all, unless there are initial inhomogeneities which lead to a net momentum in local transverse space. (This is known as the “firestreak model” [31, 33]). Boost invariance is badly broken at the beginning of the fireball evolution and such a pancake has very little in common with the scenario used in [23, 25]. One can consider Bjorken and Landau as two extremes: In the Bjorken scenario, the
nuclei originally pass through each other with minimal reinteraction and strings that stretch between colliding gluons arise in parallel to other strings. In the Landau scenario, they “stick together” or at least leave some energy in the middle.

While constructing a coordinate system around a physical symmetry is highly desirable, a physics justification would be needed for the approximation of Eq. (1). A direct measurement of $dN/dy$ is inconclusive. On the one hand, the Landau model fits a Gaussian well at all energies, with universal limiting fragmentation, as expected in [27–29]; moreover, strong violations of boost-invariance considerably lessen the HBT puzzle [36]. However, the multiplicity dependence on $\sqrt{s_{NN}}$ is not exactly that predicted in [27–29]. This by itself does not rule out the Landau scenario, as it can be accounted for by treating the initial thickness evolution with $\sqrt{s_{NN}}$ as a free parameter, as done in the Bjorken scenario.

There are two main arguments one can give for the Bjorken limit being more appropriate: The first one is that the perturbative partonic picture of the system [37, 38] makes this initial condition natural. However, even in the weakly-coupled limit, low $x$ partons could lead to a breakdown of Eq. (2) (see for example, [39, 40]). Moreover, if the initial state is strongly coupled from the beginning, one could indeed expect that it would appear much more Landau-like [41, 42] than Bjorken-like, although the degree of stopping might also depend strongly on energy and system size [43, 44]. Stopping is therefore not determined a priori, as the interaction strength at the beginning of the system’s evolution is currently a controversial topic.

The second reason is that, for mid-rapidity data, it is widely believed that the difference between Bjorken and Landau evolution is irrelevant. As is clear from [27], Landau evolution converges to Bjorken evolution after some sufficient time. The reason for this behavior is that longitudinal flow forms on the scale of $\Delta/c_s$, while transverse flow forms on a much larger scale $\sim R/c_s$ where $c_s$ is the speed of sound. Hence, since $\Delta \ll R$ for $\sqrt{s_{NN}} \gg 1$ GeV, initially the system can be considered, as indeed it is in [27], to be a purely 1D expanding “sharp step.” As again shown in [27, 29, 30], the long-term longitudinal evolution of such a system at mid-rapidity is indistinguishable from that of [29]. Hence, boost-invariant hydrodynamics can be safely used even if, at the very initial stage [25], the system is very far from boost invariance. Landau evolution at mid-rapidity can be treated as Bjorken with $\tau_0 \sim 1$ fm GeV/$\sqrt{s_{NN}}$. Perhaps, this scaling will give unrealistically low initial proper times at the LHC, but since boost-invariant simulations are only weakly sensitive to time [19], this might not be a fatal issue. This idea, however, has two flaws:

![FIG. 1. Landau initial condition (panel (a)), and actual Glauber initial conditions (panel (b)) for a typical event.](image)

![FIG. 2. (color online) Ratio of energy density at the indicated time to the initial energy density as a function of rapidity. The dashed lines show the analytical solution in (1+1)D [32] while the solid lines show our numerical calculation in (3+1)D, with Landau initial conditions, including net momentum, transverse expansion and inhomogeneities. The results from a (3+1)D hydrodynamics where Bjorken-type boost-invariant longitudinal flow is set as an initial condition [12, 13] are also shown as dotted lines. Time is normalized to units of $\Delta$ in the Landau picture and $\tau_0$ in the Bjorken picture.](image)
Additionally, the “Landau→Bjorken” reasoning assumes that the longitudinal timescale is much larger than the transverse one. This is certainly true if the transverse scale is given as a radius of a homogeneous “pancake” of radius $R$ given by an average of many events as in Fig. 1 (a). It is however less clear that such a hierarchy holds for a typical event as in Fig. 1(b). The inclusion of subnucleonic strong QCD fields [21, 45] makes this hierarchy even more dubious as the events with the strongest anisotropic coefficients would also have the most prominent “hotspots.” Potentially, this effect makes the boost-invariant picture irrelevant even for late-time hydrodynamics. The more homogeneous regions will be more similar in their longitudinal expansion to [23], while the more inhomogeneous regions would, on their own, evolve to a 3D Hubble expansion [46]. The interplay between regions of different symmetry, and local instabilities [46, 47] makes any symmetry dubious.

To investigate these effects further, one needs to perform (3+1)D calculations starting from Landau initial conditions and transverse inhomogeneities. In this work, we use an event-by-event Glauber model to generate initial-state transverse energy distributions, with the longitudinal density distribution being given by a Landau profile.

The Glauber Monte Carlo description of two colliding Au$^{197}$ nuclei at 200 GeV was used to generate the initial condition relevant to RHIC. Nucleons were distributed as per a Wood-Saxon distribution with radius 6.38 fm, and diffuseness 0.535 fm. The impact parameters were simulated randomly following a distribution of $d\sigma/db = 2\pi b$. The nucleons were assumed to have no hard-core and the condition for nucleon-nucleon collision is that the inter-nucleon distance $d$ should satisfy $\pi d^2 < \sigma_{NN}$, where $\sigma_{NN} = 42$ mb is the nucleon-nucleon cross section.

We then use the CL-SHASTA code developed in [48] to evolve this configuration according to ideal hydrodynamics, $\partial_\mu T^{\mu\nu} = 0$ with

$$T_{\mu\nu} = \left(\rho + p\right)u_\mu u_\nu + pg_{\mu\nu}$$

where $v_\nu = \frac{1}{\sqrt{1 - v_z^2}} (1, v_\tau \sin(\theta), v_\tau \cos(\theta), v_z)$

The results are publically available at

![Graph](image-url)
we concentrate on the early dynamics where the hadron gas contribution is negligible.

The energy density evolution as a function of space-time rapidity is shown in Fig. 2, which follows the trend in [27] to $\sim 20\%$ precision, as expected from correction due to transverse and elliptic flow. Hence, Fig. 2 shows a decreasing bump in $\epsilon$ (which correlates with transverse multiplicity $dN/dy \sim S_{\eta_0} 3/4$ and transverse energy $dE_T/dy \sim S_{\eta_0} e$ in the Bjorken picture [23]. Here $S \sim R^2 \sim N_{\text{part}}$ is the transverse overlap area), making these similar to boost-invariant results [23]. While comparing with the boost-invariant calculation from [12, 13] should be done with care as the physical meaning of $\Delta$ and $\tau_0$ are different, such a comparison confirms that for realistic time-scales the evolution in the two limits is significantly different. Self-quenching variables ($v_2$, and to a lesser extent the average transverse momentum $\langle p_T \rangle$), however, will be sensitive to such differences independently of freezeout.

We then calculate the longitudinal flow rapidity $y_f$ as well as the transverse flow for each slice of rapidity, averaged over the entire transverse volume, to explore boost invariance. Fig. 3 shows the ratio $y_f/y_s$ as a function of $y_s$ at various relevant times in the evolution. If the system were exactly boost invariant, $y_f/y_s$ would be strictly unity. Moreover, as Fig. 3 also shows $y_f/y_s$, averaged over both transverse volume and proper time in a $(3+1)$D evolution where boost-invariance is set as an initial condition [12, 13] $(3+1)$D dynamics acts as a very small correction to the longitudinal flow over the realistic timescale of the evolution. This shows that when Bjorken flow is added as an initial condition, $(3+1)$ dimensional hydrodynamics will be a small correction over $2+1$ dimensional hydrodynamics.

In the Landau limit the ratio does evolve towards unity as the system cools; however, it would be a gross oversimplification to treat the ratio as a constant or unity, even at significantly later times. At freezeout provided initial temperature $\sim 300$ MeV, we predict $y_f/y_s$ to be above unity by about 40% around midrapidity. At earlier stages, relevant for the formation of transverse and elliptic flow ($t \sim \epsilon_s R/c_s$ where $\epsilon_s$ is the eccentricity), these corrections are of order 50%. For comparison, we superimpose the same distributions for the 1D expansion calculated in an analytical work [32]. It can be seen that, unlike what was presumed in [28, 29], transverse expansion and local dynamics make a qualitative, and not just a quantitative effect: deviation from boost invariance oscillates and stays nearly constant rather than decreases in time when transverse expansion and anisotropies are taken into account.

This discrepancy is directly confirmed in Fig. 4 which shows that the transverse velocity as a function of the spacetime rapidity significantly violates Eq. (2), with an apparent decrease of $v_T$ as the system expands. This ap-
parently counter-intuitive behavior can be explained by the fact that when the rarefaction wave traverses the system size, the out-going shock could well experience a negative gradient at the point of maximum density (the density in front of the wave’s peak, determined by the shock wavefront, is higher than the density behind it, given by the rarefaction wave). Longitudinal expansion weakens this effect by depleting density in all of transverse space at the same time, but, as our simulation shows, in the Landau limit the full 3D flow development could be non-monotonic for part of the evolution. Note that Fig. 4 also shows that, while transverse velocity increases with $r_\perp$ as usually predicted, the presence of hotspots may make the average magnitude of $v_T$ non-zero at $r_\perp = 0$, with a rapidity dependence which follows the Gaussian profile characterising the event (its direction of course averages to zero, but it is non-zero in a typical event).

The relevance of this dynamics for transverse degrees of freedom is further elucidated in Fig. 5, which shows the dependence of $y_f/y_s$, an indicator of the degree of violation of boost invariance, on transverse flow. Thus, if the Landau initial condition is more appropriate, transverse flow and its azimuthal anisotropies form, to a certain extent, in strongly non-boost invariant regions. This is readily understood, as such regions are precisely the places where transverse gradients are larger w.r.t. longitudinal ones. Hotspots can also have a non-zero longitudinal momentum and vorticity [57] (the “firestreak”), further invalidating local boost-invariance. As Fig. 5 panel (a) however shows, this result somewhat depends on the rapidity region being explored. A restriction in flow rapidity, approximately tracking the pseudorapidity, will ensure $v_T$ is independent of the degree of boost invariance. Such a cut, however, does nothing to make the evolution examined more boost-invariant, since $y_f/y_s$ remains very well away from unity.

Fig. 5 panel (b) shows the anisotropy of the in-plane and out of plane flow, as a function of transverse flow. The combination of the results of Figs. 4, 5 indicates that dynamics relevant for transverse and anisotropic flow significantly violates boost invariance if Landau initial conditions are assumed. This is confirmed by comparing our results to the flow profile of [34, 35]: The correlation between anisotropy and flow is significantly weaker, and qualitatively different-looking in the Landau than in the Bjorken limit throughout the evolution of the fireball: Whereas in the Landau limit flow eccentricity is maximized in the middle of the fireball, in the Bjorken limit it is maximized at the edges. This is because in the Bjorken limit there is no interplay between transverse and longitudinal flow, whereas in the Landau limit the longitudinal “twist” in the $z - x$ and $z - y$ direction is developed contemporarily with the $x - y$ flow. Hence, a value of $\eta/s$ w.r.t. that fitted in papers where initial longitudinal flow was assumed [18, 21] will most likely be required to fit flow harmonic data with Landau rather than Bjorken initial longitudinal conditions. By dimensional analysis, this difference should be parametrically comparable to the deviation between the Landau and Bjorken model shown in Fig. 5 (b).

Indeed, the main shortcoming of this analysis is that the hydrodynamics was assumed to be ideal. However, it should be noted that viscosity is sensitive to differences between $y_s$ and $y_f$ examined here in a way which may be different from the intuition from boost-invariant hydrodynamics. Viscosity, shear and bulk, transforms gradients into heat. This suppresses the local structure of flow, but it also creates extra pressure that enhances flow in all directions. It has been recently realized [19] (in a model incorporating bulk viscosity, for which the first effect is reduced) the second effect’s contribution to $v_n$ can be positive, since heat creation enhances local pressure gradients, thereby boosting transverse expansion, which enhances all remaining flow structure, and this can overpower the direct degradation of flow gradients by viscosity.

Since $v_n$ is gradient projection in a purely transverse direction, for longitudinal gradients this degradation is minimized and hence viscous heating could overpower it. For boost-invariant hydrodynamics longitudinal gradients are fixed at $\sim \tau^{-1}$, and hence direct suppression of $v_n$ by viscosity overpowers viscous heating, as amply confirmed by numerical simulations [18, 20–22]. As our work shows, in Landau hydrodynamics the longitudinal gradient is much greater than $\tau^{-1}$ even at mid-rapidity. The extra boost in the gradient can slow down cooling without affecting azimuthal gradients. Thus, if initial conditions are more Landau-like, shear viscosity could be significantly higher than what is inferred by boost-invariant calculations, and could even be correlated rather than anti-correlated with initial eccentricity.

The viability of the computations performed here depends, of course, in the longitudinal structure of the event really being close to the Landau limit. Because we do not know this from first principles, and given the many undetermined parameters in a typical hydrodynamic simulation, we suggest that experimental tests specifically probing boost invariance should be performed. It is intuitively clear that in the Bjorken solution the transverse size of the system, along with other parameters, does not vary with rapidity. It is equally intuitively clear that the strong dependence of flow with rapidity produces a strong rapidity dependence of size at late times. Fig. 6 confirms this, where the average $\langle r^2 \rangle$ integrated over the transverse radius is shown as a function of rapidity. As can be seen, it approximately follows the Gaussian structure of the transverse momentum characteristic of Landau hydrodynamics [27–29], varying over orders of magnitude in the fragmentation region. In the Bjorken picture, such wide variation is excluded since the transverse size is bounded by the initial transverse size, $\sim N_{\text{part}}^{2/3}$ at all rapidities.

This quantity, in the Gaussian approximation, is related to the HBT variable $R_{\text{side}}$ [58]. This relationship is not straightforward, since $R_{\text{side}}(K)$ is defined in terms of
FIG. 5. (color online) Panel (a) $y_f/y_s$ as a function of mean transverse velocity for $|y_f| < 0.5$ (hashed red) and with no restriction on $y_f$ (solid black). Panel (b) Distribution of transverse flow anisotropy versus mean total transverse velocity for in-plane (solid black) and out-of-plane (hashed red) flow. Both are averaged over fireball volume and event sample, with the bands representing the variance over the average across events. The results for event-by-event (2+1)D simulation including initial inhomogeneities [34, 35] are also shown as points.

In the same way, the shorter longitudinal size of the Landau “pancake” in spacetime would mean that in-medium energy absorption for a fast parton (“tomographic energy loss”) for higher rapidity will be significantly weaker than in the purely transverse direction (Fig. 7 panel (a)), since the initial size in the longitudinal direction in the Landau limit will be much smaller ($\sim \Delta/\sin\theta$) than in the Bjorken limit ($\sim R/\cos(\theta)$, Fig. 7 panel (b)), and since jets will generally traverse the system faster than the build-up of longitudinal flow. Note that this distinction is sensitive to precisely the physical difference of Landau and Bjorken: In the Bjorken case the projectile and target collide transparently and continue moving at the speed of light (faster than the fast parton’s speed), while in the Landau case longitudinal motion stops until hydrodynamics sets in (parametrically slower than the fast parton’s speed).

The decrease in longitudinal size of course is balanced by the higher initial density, but away from the weakly coupled Bethe-Heitler limit, size and density do not compensate [49]. For instance, in the LPM limit the total energy lost by the parton traversing a medium of length $L$ is $\Delta E \sim \rho L^2$, while if theories with gravity duals describe jet-medium interaction, the energy lost by the parton $\Delta E \sim \rho L^m \gamma^2$ ([50] and references therein). Following the calculation of $R_{AA}$ in [51], where this exponent $m$ is...
kept arbitrary
\[ R_{AA} \simeq \left\langle \exp\left[ -\kappa \int dl \ln^{-1} \rho(x_0 + \hat{n}) \right] \right\rangle \tag{9} \]

where \( \kappa \) is a constant and \( \langle A \rangle \) integrates \( A \) over all \( x_0, \hat{n} \) and events. We can use simple geometrical scaling from Fig. 7 to approximate the trigger particle’s rapidity \( y \) by the pseudo-rapidity
\[ y \simeq -\ln \tan \left( \frac{\theta}{2} \right) \tag{10} \]

Assuming fast partons are produced at \( y_s = 0 \) (at the initial collision), and uniformly in net Bjorken \( x \), we infer that, if the jet leaves the system before significant flow develops, for \( y \gg 0 \) and in terms of \( \kappa' = \kappa \langle \rho \Delta^m \rangle \). In the limit \( y \gg 0, \Delta \ll R \)
\[ R_{AA}(y) \sim \exp[ -\kappa' \exp[ -\kappa y]] \tag{11} \]

No doubt this estimate is extremely rough, and a more quantitative estimate is the subject of a subsequent work, but, unless the bulk of jet energy loss is due to non-tomographic effects (such as initial [52] and fragmentation [53] effects) or jet energy loss is not approximately collinear (as is generally believed), we can expect that the jet suppression parameter \( R_{AA}(p_T, y) \) [49] to rise steeply with the rapidity of the trigger particle \( y \). In contrast, since in the Bjorken limit jets are still produced during the initial hard scattering \( y_s = 0 \) for all \( y \), the corresponding quantity to Eq. 11 is \( R'_{AA} \sim \exp[ -\kappa'] \) independently of \( y \), since the parton keeps traversing the medium even at \( y \gg 1 \). In this limit, \( R'_{AA} \) is not a good approximation as longitudinal expansion is neglected [50], but one expects that tomographic energy loss should not decrease in rapidity even for very high rapidities, and may in fact increase if the \( m \) parameter [51] is large enough for the extra path (Fig. 7 panel (b)) to compensate for decreased in-medium parton density. Thus, jet energy loss dependent on rapidity could be a decisive and direct test of boost invariance. While experimental results do tend to favor a Bjorken picture rather than the picture examined in this paper [54, 55], a systematic study relating \( dN/dy \) to \( R_{AA} \) in rapidity, as well as a quantitative calculation of \( R_{AA} \) in both limits, is necessary for a definite conclusion.

Observables such as the correlator studied in [56] or polarization [57] could give further tests.

In conclusion, we have shown that, provided the system is Landau-like in its initial stages, it will not, as commonly expected, evolve to a Bjorken-like stage within realistic timescales. Furthermore, the deviation from boost invariance is directly correlated with the development of transverse and elliptic flow, the characteristic signatures used to demonstrate and quantitatively study the hydrodynamics of the quark-gluon plasma. In view of these results, the transport properties of the medium created in heavy ion collisions could be considerably different from those usually assumed.

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FIG. 7. A schematic representation of tomography in a Landau (panel (a)) vs Bjorken collision (panel (b)) for pairs of jets produced at higher rapidity (dashed lines with arrows) and mid-rapidity (dotted lines with arrows). While the quantitative result depends on the details of the quenching model (see for example [50]), it is clear $R_{AA}$ will rapidly increase with rapidity in the Landau limit.

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