A semi-analytical perspective on massive galaxies at $z \sim 0.55$

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ABSTRACT

The most massive and luminous galaxies in the Universe serve as powerful probes to study the formation of structure, the assembly of mass, and cosmology. However, their detailed formation and evolution is still barely understood. Here we extract a sample of massive mock galaxies from the semi-analytical model of galaxy formation (SAM) GALACTICUS from the MULTIDARK-GALAXIES by replicating the CMASS photometric selection from the SDSS-III Baryon Oscillation Spectroscopic Survey (BOSS). The comparison of the GALACTICUS CMASS-mock with BOSS–CMASS data allows us to explore different aspects of the massive galaxy population at $0.5 < z < 0.6$, including the galaxy–halo connection and the galaxy clustering. We find good agreement between our modelled galaxies and observations regarding the galaxy–halo connection, but our CMASS-mock overestimates the clustering amplitude of the two-point correlation function due to a smaller number density compared to BOSS, a lack of blue objects, and a small intrinsic scatter in stellar mass at fixed halo mass of $<0.1$ dex. To alleviate this problem, we construct an alternative mock catalogue mimicking the CMASS colour–magnitude distribution by randomly down-sampling the SAM catalogue. This CMASS-mock reproduces the clustering of CMASS galaxies within $1\sigma$ and shows some environmental dependency of star formation properties that could be connected to the quenching of star formation and the assembly bias.

Key words: galaxies: evolution -- galaxies: haloes -- cosmology: theory -- dark matter.

1 INTRODUCTION

The most luminous and massive galaxies in the Universe serve as powerful probes to study the formation of structure, the assembly of mass and cosmology, but their detailed formation and evolution, especially their connection to feedback processes, quenching of star formation, or the assembly bias is still not sufficiently understood or quantified (Tinker et al. 2013; Wechsler & Tinker 2018). The Sloan Digital Sky Survey SDSS-III/Baryon Oscillation Spectroscopic Survey (BOSS, Schlegel, White & Eisenstein 2009; Eisenstein et al. 2011; Dawson et al. 2013) was dedicated to studying properties of the large-scale distribution of massive galaxies and provides a well-studied sample of $\sim 1.5$ million luminous red galaxies (LRGs). The BOSS sample is divided into two: a low-redshift (LOWZ) and a high-redshift sample (CMASS, stands for ‘constant mass’), respectively.

The CMASS sample covers a wide redshift in the range $0.43 < z < 0.75$ exhibiting a peak in comoving number density of $n \sim 3.4 \times 10^{-4} \ h^3 \text{Mpc}^{-3}$ at $z \sim 0.5$. The stellar mass function (SMF) evolves very little in this redshift range suggesting that CMASS galaxies are passive and show almost no ongoing star formation.

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A non-evolving sample of massive galaxies provides an excellent ‘cosmic laboratory’ to study galaxy formation and evolution as shown by Bernardi et al. (2016), Montero-Dorta et al. (2016), and Montero-Dorta, Bolton & Shu (2017a), and their link to cosmology via e.g. the large-scale structure (LSS) distribution and clustering of BOSS galaxies studied by Chuang et al. (2016), Rodríguez-Torres et al. (2016), and Guo, Yang & Lu (2018). BOSS LRGs were repeatedly used to determine fundamental cosmological parameters (Cuesta et al. 2016; Gil-Marín et al. 2017; Ross et al. 2017) and to put cosmological models to the test (e.g. Anderson et al. 2014; Beutler et al. 2014; Alam, Ata & Bailey 2017; Sullivan, Wiegand & Eisenstein 2017; Mueller et al. 2018). Furthermore, because the sample addresses the most luminous and red galaxies, they act as an important probe to close the gap in understanding the link between dark matter haloes and massive galaxies (Leauthaud et al. 2012; Nuza et al. 2013; Guo et al. 2014; Favole et al. 2016; Saito et al. 2016).

At low redshift LRGs are known to populate the most massive haloes located in denser regions such as the centre of clusters and superclusters (Lietzen et al. 2012). That makes them particularly interesting to study, because they give clues to the assembly of the most massive structures, the formation of haloes, and their connection to their associated galaxies. Thereby the ratio of their stellar to halo masses as a function of halo mass (SHMF) allows for exploring the galaxy–halo connection and the formation and evolution of those galaxies in dark matter haloes of a certain mass range. Or equally, what halo mass is related to a galaxy that produced a certain stellar mass over a certain time. From a more cosmological point of view the relation shows how galaxies trace dark matter and how its density field is distributed. 1 Interestingly, the haloes at intermediate masses produce stars most efficiently, the haloes at intermediate masses produce stars most efficiently, and their link to cosmology via e.g. the large-scale structure (LSS) distribution and clustering of BOSS galaxies studied by Chuang et al. (2016), Rodríguez-Torres et al. (2016), and Guo, Yang & Lu (2018). BOSS LRGs were repeatedly used to determine fundamental cosmological parameters (Cuesta et al. 2016; Gil-Marín et al. 2017; Ross et al. 2017) and to put cosmological models to the test (e.g. Anderson et al. 2014; Beutler et al. 2014; Alam, Ata & Bailey 2017; Sullivan, Wiegand & Eisenstein 2017; Mueller et al. 2018). Furthermore, because the sample addresses the most luminous and red galaxies, they act as an important probe to close the gap in understanding the link between dark matter haloes and massive galaxies (Leauthaud et al. 2012; Nuza et al. 2013; Guo et al. 2014; Favole et al. 2016; Saito et al. 2016).

1From the density field the corresponding power spectrum can be constructed and from that cosmological parameter determined. One can see that this simple relation between stellar and halo mass is indeed a powerful constraint.
algorithm guarantees for an extension towards the bluer colours and the so-called ‘blue-cloud’ (BC) galaxies can enter the CMASS sample. In our study we use BOSS data from Data Release 12 (hereafter BOSS-CMASS DR12; Alam et al. 2015). The following colour–magnitudes cuts are used to select the CMASS galaxies:

\[ d_\perp > 0.55, \]  
\[ i < 19.86 + 1.6(d_\perp - 0.8), \]  
\[ 17.5 < i < 19.9, \]  
\[ r - i < 2, \]  
\[ i_{\text{psf}} - i_{\text{mod}} > 0.2 + 0.2(20.0 - i_{\text{mod}}), \]  
\[ z_{\text{psf}} - z_{\text{mod}} > 9.125 - 0.46z_{\text{mod}}, \]

where \( d_\perp \) is called the ‘composite colour’ with

\[ d_\perp = (r - i) - (g - r)/8.0, \]

\[ g, r, i \text{ are the cmodel magnitudes in the AB-system, } i_{\text{mod}} \text{ and } z_{\text{mod}} \text{ refer to model magnitudes, } i_{\text{psf}} \text{ is the fiber magnitude, and } z_{\text{psf}} \text{ are the PSF magnitudes. For more information about the set of colour–magnitudes cuts consult the BOSS–CMASS DR12 target selection webpage.}^2 \]

Equation (1) isolates high-redshift objects; equation (2) is a sliding magnitude cut that selects the brightest or more massive galaxies with redshift; equation (3) defines the faint and bright limits and equation (4) protects from some outliers. Equation (5) ensures a high-redshift measurement success rate and equations (6) and (7) perform a star-galaxy separation.

We use the latest LSS catalogue\(^1\) (Reid et al. 2016) from the SDSS3 Data Science Archive Server which was cross-matched with the Portsmouth\(^4\) passive galaxy sample to include stellar masses. The stellar masses were generated via a post-processing step using the stellar population models of Maraston (2005) and Maraston et al. (2009) to perform a best fit to observed ugriz-magnitudes (Fukugita et al. 1996).

We use Planck cosmology and assume a Chabrier (2003) initial mass function (IMF). The Portsmouth galaxy product assumes a WMAP7 flat ΛCDM cosmology with a dimensionless Hubble parameter of \( h = 0.7 \) (White et al. 2011, same as in the entire BOSS pipeline) and Kroupa (2001) IMF. Therefore, we correct their stellar masses from WMAP7 to Planck cosmology.\(^5\) We further convert the stellar masses to match the assumed IMF of MULTIDARK-GALAXIES models (Chabrier 2003), with the following conversion: \( \log_{10} M_{\text{Chabrier}} = \log_{10} M_{\text{Kroupa}} - 0.03925 \) (see table B1 in Lacey et al. 2016).

For the data reduction we use the same approach as Rodríguez-Torres et al. (2016), described in their section 2. In order to account for redshift failure and fiber collision we apply weights given by Anderson et al. (2014) using equation (9) in Rodríguez-Torres et al. (2016). This results in a total number of 818 817 observed CMASS galaxies (entire redshift range). For this work we select a subsample of galaxies in the range \( 0.5 < z < 0.6 \), which guarantees for maximal completeness in number density (Guo et al. 2018), leaving us with a catalogue of 423 671 galaxies to study. We use this selection to compute the SMF and clustering of the observed galaxies using the Planck parameters as a fiducial cosmology. We also extract the bias and number density from this sample to construct a halo abundance matching (HAM) on the BigMDPL simulation that describes these observations. Furthermore, the BOSS survey covers around \( \sim 9600 \text{deg}^2 \) of the sky which corresponds to a volume of \( \sim 4.147 \times 10^{9} \text{Mpc}^3 \) within our redshift range and assumed cosmology.

\[ M_{\text{ref}}(\leq R_{\text{ref}}) = \Delta_{\text{ref}}\rho_{c} \frac{4\pi}{3} R_{\text{ref}}^3, \]

where \( \Delta_{\text{ref}} = \Delta_{\text{BN98}} \) for \( M_{\text{BN98}} \) with \( \Delta_{\text{BN98}} \) being the virial factor as given by the equation (6) of Bryan & Norman (1998), \( \rho_{c} \) being the critical density of the Universe, and \( R_{\text{ref}} \) being the corresponding halo radius for which the interior mean density matches the desired value on the right-hand side of equation (9). For information on the models’ calibration and intrinsic constrains, we refer to the MULTIDARK-GALAXIES data release paper Knebe et al. (2018, section 2.2 and table 1).

Galacticus returns luminosities, \( L \) in the SDSS ugriz-bands at the zero-point of the AB-magnitude system in units of \( 4.4659 \times 10^{19} \text{WHz}^{-1} \). We apply \( M_{\text{AB}} = -2.5\log_{10}L \) to convert \( L \) to absolute magnitudes \( M_{\text{AB}} \) in each filter band. The filter band was by default blue-shifted to the redshift of the galaxy, meaning that in order to compute the apparent magnitude one must add not only the distance modulus, but also a factor of \(-2.5\log_{10}(1 + \delta)\) to account for the compression of the photon frequencies at \( \delta = 0.56 \). For the sake of simplicity and to avoid introducing additional uncertainties we use this approximation (Blanton & Roweis 2007, see section 4), but do

\[ \text{The galaxy catalogue is publicly available on www.cosmosim.org and www.skiesanduniverses.org.} \]

\( ^2 \)\url{http://www.sdss.org/dr12/algorithms/boss_galaxy_zs/}

\( ^3 \)\url{https://data.sdss.org/sas/dr12/boss/ls/}

\( ^4 \)\url{http://www.sdss.org/dr13/spectro/galaxy_portsmouth/}

\( ^5 \)In order to translate between cosmologies we assume the simple relation of \( \log_{10} M_{\text{Planck}} = \log_{10} M_{\text{WMAP}} + \alpha \log_{10} \frac{\Omega_{\text{Planck}}}{\Omega_{\text{WMAP}}} \), with \( M_{\text{P}} \) being the stellar mass and \( D_c \) the comoving distance within a certain cosmology.
not apply the full $K$-correction. This results in

$$m_{\text{AB}} = M_{\text{AB}} + DM(z) - 2.5 \log_{10}(1 + z_0), \quad (10)$$

with $m_{\text{AB}}$ being the observed apparent magnitude in the AB-system and $DM(z) = 5 \log_{10}(D_L/10\text{pc})$ the distance modulus with $D_L$ as luminosity distance at the redshift $z = 0.56$ in parsec.

3 SAMPLE SELECTION AND COLOUR–MAGNITUDE EVALUATION

In this section we show how we extracted a CMASS-mock sample from the MDPL2-Galacticus catalogue. Since we deal with modelled galaxy properties we only use a limited set of colour–magnitude selection cuts, equations (1)–(4), because the simulation does not distinguish between model and cmodel magnitudes.\footnote{‘model’ and ‘cmodel’ refer to different approaches of how magnitudes have been generated through the photometric pipeline of SDSS.}

In order to test our CMASS-mock samples we compare on the one hand to observed CMASS galaxies from the Portsmouth merged galaxy catalogue of the 12th data release (referred to as CMASS DR12) in the redshift range of $0.5 < z < 0.6$ (the most complete range in terms of stellar masses), which corresponds to a comoving number density of $n = 1.02 \times 10^{-4} \text{ Mpc}^{-3}$ at redshift $z \approx 0.55$ in our adopted cosmology. And on the other hand we extract two more CMASS-mock samples aiming at reproducing the colour–magnitude selection using other galaxy properties as stellar mass. We do that because luminosities or colours are not always available for modelled galaxy samples, especially if they are as large as MDPL2. Furthermore, we can assess the colours and luminosities of our SAM by comparing it with a sample selected by applying a high mass cut corresponding to a conservative confidence cut.

Therefore we create a second and a third CMASS-mock sample by matching the number density and the stellar mass distribution of the observed sample CMASS DR12, or by applying a high stellar mass cut corresponding to CMASS galaxies as reported by Maraston et al. (2013), respectively. We summarize our sample selection in the following list:

- **Gal-all**: resulting full sample of $\sim 1.8 \times 10^9$ galaxies after applying a confidence cut in stellar masses\footnote{This stellar mass threshold corresponds to a conservative confidence cut above the output of the model can be trusted – see MULTIDARK-GALAXIES release paper for details.}: $M_*> 10^{10.5} \text{ M}_\odot$; this is the entire sample of Galacticus at $z = 0.56$

- **Gal-cols**: colour-selected sample; the observational CMASS colour–magnitude selection, equations (1)–(4), described in Section 2.1, has been applied\footnote{We use dust-extincted luminosities in our study because we compare with observations. If we would use non-dust corrected luminosities instead, we would find very small differences of about $\Delta M_{\text{AB,ext}} \sim 0.1$--0.2 mag in gri-bands compared to dust-extincted magnitudes.}

- **Gal-dens**: number density-selected sample: the number density of BOSS-CMASS DR12 ($n_{\text{CMASS}} = 1.02 \times 10^{-4} \text{ Mpc}^{-3}$) was matched via randomly down-sampling the red population of Gal-all sample SMF at $z = 0.56$. The red population was selected with a cut in colour as introduced by Guo et al. (2013, equation 7):

$$r - i > 0.679 - 0.082 (M_i - 20). \quad (11)$$

We use equation (11) instead of a simple cut in red–blue separation as $(g - i) > 2.35$ because otherwise we would exclude a significant amount of galaxies at $M_* \sim 10^{11.2} \text{ M}_\odot$ and fail to calculate the true SMF. After applying the colour selection, we calculate the fraction between the densities of the SMFs $\Phi_{\text{CMASS DR12}}$ and Galacticus and use it to compare to a random distribution, $S_{\text{rand}}$, in the range [0, 1]:

$$S_{\text{rand}} < \Phi_{\text{CMASS DR12}} / \Phi_{\text{Galacticus}}, \quad (12)$$

A galaxy enters the sample if the condition in equations (11) is fulfilled, otherwise it is discarded.

- **Gal-mass**: stellar mass-selected sample; we apply a stellar mass $M_* > 10^{11.2} \text{ M}_\odot$ on Gal-all (see Maraston et al. 2013).

Table 1 summarizes the properties of our observational and modelled CMASS samples. We show the total number of galaxies $N_{\text{gal}}$, total number fractions of ‘centrals’, ‘satellites’, and ‘orphan (satellites)’,\footnote{‘Orphan’ or ‘orphan satellite’ is a technical term in semi-analytical modelling, referring to satellites that lost their dark matter haloes due to the interaction with their central galaxies or other reasons such as resolution limits of the halo finder.} number densities $n$, and effective volumes $V_{\text{eff}}$. Although the $N_{\text{gal}}$ and $n$ are different in each CMASS-mock sample, the fraction of centrals ($f_{\text{cen}}^{\text{total}} \sim 0.9$) and satellites ($f_{\text{sats}}^{\text{total}} \sim 0.1$) are almost identical and agree perfectly with the observation (Guo et al. 2014; Rodríguez-Torres et al. 2016). However, we note that the number density of the Gal-cols sample $n_{\text{Galacticus}} = 0.30 \times 10^{-4} \text{ Mpc}^{-3}$ roughly corresponds to only 1/3 of the BOSS-CMASS DR12 with $\sim 1.02 \times 10^{-4} \text{ Mpc}^{-3}$. The discrepancy in the numbers and its consequences will be discussed later. In the following section we perform sanity checks on our Gal-cols CMASS-mock by directly comparing with BOSS-CMASS DR12 data. Note that to avoid crowding we only show Gal-cols and the observational sample in the figures.

3.1 Gal-cols: the composite colour $d_1$

The composite colour $d_1$ is a colour combination defined in equation (8) and the key colour selection parameter for CMASS galaxies involving three bands: $g$, $i$, and $r$. Fig. 1 presents the colour–magnitude diagram (CMD) where $d_1$ is shown compared to the observed $i$-band magnitudes, $m_{\text{AB}}$. This is the first and most important sanity check we use to assess our colour selection. The CMASS-colour–magnitude selection described in equations (1) and (3) are shown as a polygon-shaped area with a thin solid black line, where all galaxies within this area enter the selection. The Galacticus CMASS sample, Gal-cols, is shown in black filled coloured contours and BOSS-CMASS DR12 in red dashed empty contours. We show the parameter space of the entire set of galaxies, Gal-all, as grey logarithmic binned hexagons in the background to point out that the CMASS sample is only a tiny fraction of the total set of galaxies that Galacticus provides. For the contour figures we use throughout this work the following confidence levels in per cent: (2.1, 13.6, 31.74, 68.26, 95, 99.7).

The histogram panels on the top and on the right-hand side give information about the distribution of galaxies along the binned
Table 1. The table summarizes the properties of the observed and modelled galaxy samples used in our study. Column (i) shows the name of the publicly available galaxy catalogue we extracted a sample from, (ii) gives the label of the corresponding sample throughout this paper, and (iii) its total number of galaxies \( N_{\text{gal}} \). The corresponding fraction of central, satellite, or orphan galaxies can be found in (iv) \( f_{\text{total}}^{\text{centrals}} \) for centrals, (v) \( f_{\text{total}}^{\text{orphan sats}} \) for all satellites (non-orphans + orphans), and (vi) \( f_{\text{total}}^{\text{orphans}} \) for orphan satellites (the fraction of orphan satellites is calculated with respect to the total number of satellites), respectively. The number density \( n \) of each sample and the effective volume \( V_{\text{eff}} \) can be found in Column (vii) and (viii), respectively. Column (ix) provides comments on the selection. For the observational sample we select BOSS-CMASS DR12 galaxies in the redshift range of \( 0.5 < z < 0.6 \) and label the sample CMASS DR12. For the modelled galaxies we show the entire galaxies sample above a confidence cut in stellar mass of \( M_\ast > 10^{10.7} \, M_\odot \); [Gal-all] and the following CMASS-mock samples: [Gal-cols], [Gal-dens], and [Gal-mass] at redshift \( z = 0.56 \) (which matches the median redshift of the full CMASS sample). To extract [Gal-cols] the standard set of CMASS colour–magnitude cuts from equations (1)–(4) was applied. For [Gal-dens] we used a down-sampling algorithm shown in equations (11) and (12), where we selected randomly galaxies from the red population that matched the number density of CMASS DR12. For [Gal-mass] a stellar mass cut at \( M_{\ast} > 10^{11.24} \, M_\odot \) was applied according to the findings of Maraston et al. (2013).

| Data          | Sample name | \( N_{\text{gal}} \) Total | \( f_{\text{total}}^{\text{centrals}} \) (\( N_{\text{gal}} \)) | \( f_{\text{total}}^{\text{orphan sats}} \) (\( N_{\text{gal}} \)) | \( f_{\text{total}}^{\text{orphans}} \) (\( N_{\text{gal}} \)) | \( n \times 10^4 \) [Mpc\(^{-3}\)] | \( V_{\text{eff}} \times 10^4 \) [Mpc\(^3\)] | Remark |
|---------------|-------------|-----------------------------|---------------------------------------------------------------|---------------------------------------------------------------|---------------------------------------------------------------|--------------------------------|-----------------------------|---------|
| BOSS-CMASS DR12 | CMASS DR12  | 423 671                     | ~0.900                                                        | ~0.100                                                        | –                                                             | 1.02                           | 4.147                       | entire set of galaxies |
| MDPL2-Galacticus | Gal-all     | 1844 542                    | 0.792                                                         | 0.020                                                         | 0.020                                                         | 5.737                          | 3.212                       | \( M_\ast > 10^{10.7} \, M_\odot \) |
| MDPL2-Galacticus | [Gal-cols]  | 95 683                      | 0.901                                                         | 0.089                                                         | 0.112                                                         | 0.30                           | 3.212                       | set of colour–magnitude cuts: equations (1)–(4) |
| MDPL2-Galacticus | [Gal-dens]  | 314 083                     | 0.848                                                         | 0.151                                                         | 0.171                                                         | 1.02                           | 3.212                       | red-blue cut using Guo et al. (2013, equation 7) |
| MDPL2-Galacticus | [Gal-mass]  | 129 109                     | 0.899                                                         | 0.101                                                         | 0.118                                                         | 0.40                           | 3.212                       | down-sampled with SMF at \( z = 0.56 \) |

Figure 1. CMD for the modelled sample [Gal-cols] (filled coloured contours) at \( z = 0.56 \) and BOSS-CMASS DR12 galaxies in the range of \( 0.5 < z < 0.6 \) (red dashed contours) for observed frame \( d_\perp - \text{colour} \) compared to observed apparent \( i \)-band magnitudes \( m_{\text{AB}} \). The solid black polygon-shaped area represents the CMASS colour–magnitude cuts, the grey hexagons represent the total population of galaxies, [Gal-all]. Modelled and observed galaxies are in very good agreement with each other.

3.2 [Gal-cols]: colour–colour and colour-mass diagrams

We show in the upper panel of Fig. 2, the \((r - i)\) versus \((g - i)\) colour–colour diagram. The observed CMASS data (referred to as CMASS DR12) extends over a much larger region in the \((r - i)\) and \((g - i)\) than GALACTICUS [Gal-cols]. This is most likely due to the fact that uncertainties (i.e. photometric errors) are not implemented in the model, so no artificial blurring was produced compared to the observations. We also note that the centroid of the [Gal-cols] distribution is located at slightly redder colours \([r - i] \sim 1.05 \) and \([g - i] \sim 1.7\) than those of the observations and the location of the intrinsic ‘red sequence’ (RS) from Montero-Dorta et al. (2016). The intrinsic RS is the narrow sequence of massive red galaxies modelled as an extended Gaussian and is constituted as the counterpart to the ‘blue cloud’ which is a more heterogeneous population consisting of galaxies with bluer colours Montero-Dorta et al. (2016). We further include the composite colour \( d_\perp - \text{cut} \) as a horizontal, and a common separation of red and blue galaxies, \((g - i) = 2.35\) (Masters et al. 2011), as a vertical thin solid black line.

We show in the lower panel of Fig. 2 the \((g - i)\) colour dependence on stellar mass. The [Gal-cols]’ galaxies are slightly more massive bars for BOSS-CMASS DR12. The histogram of [Gal-all] is not shown for reasons of overcrowding.

While the majority of the modelled galaxies lies outside the CMASS selection, we nevertheless report that a substantial number enter it. Their numbers can be found in Table 1 under the label [Gal-cols]. We like to remark that Maraston et al. (2013, fig. 17) report similar results for their adopted SAM. One can see in the histogram panels that GALACTICUS’ number of galaxies in each bin is in general higher and less spread across the axes compared to the observations. In the next section we will discuss this issue in form of a colour–colour diagram in more detail.
SAM CMASS-mocks 1321

4 SAMPLE COMPARISON

Since luminosities are due to many uncertainties involved in the SPS fitting (see e.g. Conroy et al. 2009) much more complicated to model than masses, SAMs often reproduce only SMFs to a certain degree. Observations need to go the other way: fluxes have been measured and stellar spectral energy distribution (SED) fitting performed to assume stellar masses (Maraston et al. 2006). Usually a huge computational effort was brought forward to create luminosities for... SAMs applied to volumes as large as MultiDark. Therefore, we want to investigate the variation in our samples of selecting CMASS galaxies by colour (as done in observations) versus by other galaxy properties as stellar mass (as mentioned in the previous section) using the fiducial plots from Section 3 once again.

4.1 Colour–magnitude diagram

Fig. 3 presents in the upper panel the CMD (as in Fig. 1) for the three modelled samples comparing observed frame $d_{L}$ colours to observed $i$-band magnitudes, $m_{ABi}$. A large part of the galaxies of the Gal-dens sample and Gal-mass sample lie outside the polygon reflecting the colour selection. The peak in magnitudes of Gal-dens is shifted 0.3 mag to fainter luminosities compared to Gal-cols and extending into the low-luminosity regime. Gal-mass agrees pretty well with Gal-cols, where its peak is located exactly on the CMASS edge with $m_{ABi} = 19.9$.

4.2 Colour–colour diagram

In the middle panel of Fig. 3 we show the colour–colour diagram for observed colours $(r - i)$ versus $(g - i)$ (as in Fig. 2 lower panel). The horizontal thin solid black line represents the $d_{L}$-cut and the vertical black line the red–blue separation of $(g - i) = 2.35$. The filled yellow circles show modelled RS of different $i$-band magnitude slices from Montero-Dorta et al. (2016). The three samples are in very good agreement with each other, but we can see that the galaxies of Gal-dens and Gal-mass extend slightly towards ‘bluer’ colours.

4.3 Colour–mass diagram

In the lower panel of Fig. 3 we show observed frame colour $(g - i)$ versus $M_{i}$ (as in Fig. 2, lower panel). This figure shows that the mass distribution of the three samples is quite different. Gal-dens, which has the same number density as BOSS, does not coincide with the sample selected by colour, Gal-cols. However, the galaxies of the Gal-dens sample can be bound within the contours of BOSS-CMASS DR12. Alternatively, a high-mass cut in stellar mass can be used to mimic the Gal-cols sufficiently. The next paragraph is dedicated to studying the distribution of stellar masses in our samples in more detail.

4.4 Stellar mass function

In Fig. 4 we present the SMFs at redshift $z = 0.56$ for the total number of model galaxies from GALACTICUS Gal-all sample, as well as the CMASS-mocks: Gal-cols, Gal-mass, and Gal-dens compared to CMASS DR12 (filled yellow circles). We state errors in the $y$-axis of the density functions as $\sigma_{i} = \sqrt{N_{i}}$, where $i = 0,...,\text{nbins}$, $y_{i}$ stands for the data on the $y$-axis, $N_{i}$ for the number of galaxies in each bin, and $\text{nbins}$ for the number of bins.

As expected, the different CMASS-mock samples of GALACTICUS agree very well with each other. They show only slight variation at the high-mass end compared to Gal-cols due to the colour selection which excludes a few bright objects. Those could enter in Gal-dens and Gal-mass because no colour selection was performed. At intermediate masses all three samples agree perfectly with each other, but their abundances lie slightly beyond the observations. At lower masses we report that the Gal-cols sample shows the same typical shape of incompleteness in the stellar mass function as e.g. Rodríguez-Torres et al. (2016, fig. 3) for the...
Figure 3. Fiducial plots discussed in Section 3 including all three CMASS-mocks of GALACTICUS at redshift $z = 0.56$: Gal-cols (filled coloured contours), Gal-dens (red dashed contours), and Gal-mass (yellow solid contours) compared to CMASS DR12 (dotted–dashed grey contours) within the range $0.5 < z < 0.6$. Top: CMD. The solid black polygon-shaped area represents the CMASS colour–magnitude selection. Middle: observed colour $(r - i)$ versus $(g - i)$. The horizontal black line represents the $d_{\perp}$-cut and the vertical black line in the same panel the red–blue separation of $(g - i) = 2.35$. The filled yellow circles represent the modelled RS of different $i$-band magnitude slices from Montero-Dorta et al. (2016). Bottom: $(g - i)$ versus $M_{*}$.

Figure 4. GALACTICUS’ stellar mass functions for the entire sample of galaxies (thin black line) and CMASS-mock samples: Gal-cols (blue solid line), Gal-dens (red dashed line), and Gal-mass (grey dotted–dashed line) at redshift $z = 0.56$ compared to CMASS DR12 Portsmouth merged catalogue (filled yellow circles) in the range of $0.5 < z < 0.6$. Their error bars are located within the size of the markers. In order to improve the readability of the figure, we removed the vertical line dropping to zero at $M_{*} > 10^{11.24}$ $M_{\odot}$ due to the stellar mass cut applied on Gal-mass.

BIGMULTIDARK BOSS light-cone (BIGMD-LC) or Maraston et al. (2013).

In summary we have shown that using a simple cut in stellar masses provides a good approximation for the observed CMASS sample. A number density sample (created with a down-sampling algorithm) draws the SMF of CMASS perfectly, but permits bluer and low-mass objects to enter the sample. Those objects have fainter $i$-band magnitudes than CMASS as seen in Fig. 3 upper panel. However, their colours and stellar masses are still in agreement with CMASS as shown in the middle and lower panel of Fig. 3.

In the following sections we will come back to the question if a CMASS-mock can be selected by other properties than colours and magnitudes and assess if a colour selection provides a more valid sample that a simple cut in stellar mass particularly for our SAM.

Addressing a fully red population is crucial if one wants to study CMASS galaxies, and therefore we study the RS population and its $i$-band luminosity in the next paragraph.

4.5 Luminosity function

In Section 3.2 we briefly mentioned the RS population of CMASS galaxies. Now we want to discuss this topic in more detail and investigate if GALACTICUS’ CMASS-mock galaxies also exhibit such a population. The RS can be found in observations as a sort of irregular blob in the $(r - i)$ versus $(g - i)$ parameter space, elongated across the $(g - i)$-axis due to the $g$-band magnitudes higher error sensitivity. Montero-Dorta et al. (2016) developed an analytic method to model the RS luminosity function (LF) and constrained Schechter-fit parameters. We mimic GALACTICUS’ RS samples by selecting red galaxies by applying equation (11) to Gal-cols, Gal-dens, and Gal-mass, respectively. In Fig. 5 we compare GALACTICUS’ CMASS-mock samples to the best fit of Montero-Dorta et al. (2016) at $z = 0.555$. The CMASS-mocks were further blue-shifted to the same redshift using an approximated $K$-
correction of $-2.5\log_{10}(1+z)$ (Blanton & Roweis 2007) to fit the redshift of the Schechter function.\footnote{The fit uses \textsc{boss} data which were deconvolved from photometric errors and selection effects and show the raw, uncorrected, observed luminosity function. Photometric errors blur the colour–colour distribution (see the middle panel in Fig. 3), therefore objects scatter in and out of the selection boundaries leading to the observed disagreement between the results of \textsc{cmass} DR12 (filled yellow circles) and the intrinsic red-sequence from Montero-Dorta et al. (2016, thin grey dashed line).}

We report that the reddest galaxies of \textsc{galacticus} exceed the LF of the observations and the Schechter-fit of about 0.40 and 0.25 mag, respectively, at the bright end. At the faint end all three \textsc{cmass}-mock samples poorly reproduce the Schechter-fit and their LF can respectively, at the bright end. At the faint end all three \textsc{cmass}-mock samples poorly reproduce the Schechter-fit and their LF can 

\section{Results}

In this section we present our results for the \textsc{cmass}-mock samples \textsc{gal-cols}, \textsc{gal-mass}, and \textsc{gal-dens} of \textsc{galacticus}. We show SHMFs, halo occupation distributions (HODs), and projected two-point correlation functions (2pCFs).

\subsection{Galaxy–halo connection}

The \textsc{galacticus} model assumes virial overdensities to define halo masses, but the measurements we want to compare to use $\Delta_v = 200$, where $c$ refers to the critical overdensity. Therefore, we convert the halo masses $M_{\text{vir}}$ of our samples to the halo mass of our references $M_{200c}$ following Lokas & Mamon (2001, section 2.1). Particularly, we use their equation (8) to calculate the ratio of the halo masses $P_{M_{\text{halo}}}/M_{\text{vir}}$ which depends on the halo concentration parameter $c_{\text{NFW}}$ as defined by Navarro–Frenk–White (NFW, Navarro, Frenk & White 1997). Since the \textsc{galacticus} model does not provide this quantity nor the virial radius as outputs, we estimate the values using the fitting formula of Klypin et al. (2016, equation 24) and the corresponding values in Table 2 for $z = 0.50$. We calculate the $P_{M_{\text{halo}}}/M_{\text{vir}}$ for each galaxy separately, however the median over all ratios is $P_{M_{\text{halo}}}/M_{\text{vir}} = 0.884 \pm 0.002$. Our estimated NFW concentration parameters can be found roughly in the range of $4 \leq c_{\text{NFW}} \leq 6$ for $10^{13} < M_{200c} < 10^{15.5} \text{M}_\odot$.

Note further that we refer to a ‘central halo’ as the top-level dark matter halo in a certain merger tree and to ‘central galaxies’ or ‘centrals’ as the galaxies which reside in the centre of that haloes. From hereafter we exclude all orphan satellites because in the \textsc{galacticus} model they are not connected to the current central halo anymore, but point to the dark matter halo they belonged to in the past (see Knebe et al. 2018, A2 for clarification). Furthermore, their positions are not traced in the \textsc{galacticus} model, but are assigned to the central galaxies they have been associated to previously. This introduces uncertainties when calculating correlation functions which we avoid by excluding them.

\subsection{Stellar to halo mass ratio $M_*/M_{200c}$}

In the upper panel of Fig. 6, we show SHMF of our \textsc{cmass}-mocks for central galaxies only (hereafter ‘centrals’) compared to the \textsc{hama} model from Rodriguez-Torres et al. (2016) based on the \textsc{bigmultidark} simulation box with $2.5\times10^{-3}$ Gpc side-length and clustering results from \textsc{boss}–\textsc{cmass} light-cone (\textsc{bigmdlc}, a mock light-cone constructed with the sub-halo abundance matching modelling technique (\textsc{sham}) which reproduces \textsc{boss}–\textsc{cmass} DR12 large-scale structure catalogue perfectly) within 0.5 $< z < 0.6$. We further compare our \textsc{sam} data to a compilation of various \textsc{hama} realizations from Behroozi et al. (2013)\footnote{The data were modified to match the cosmology and initial mass function previously. This introduces uncertainties when calculating correlation functions which we avoid by excluding them.} at $z \approx 0.55$ and weak-lensing measurements from the Canada–France–Hawaii Telescope (CFHT) Stripe 82 from Shan et al. (2017) within 0.4 $< z < 0.6$, respectively. The additional $y$-axis on the right represents the estimated values for the NFW profile halo concentration, $c_{\text{NFW}}$, for the two mock samples, \textsc{gal-cols} and \textsc{gal-dens}, respectively.

Note that we do not show an additional right axis for \textsc{gal-mass} because its values are similar to \textsc{gal-cols}. We report that our \textsc{cmass}-mocks are in very good agreement with both, \textsc{bigmdlc} and weak-lensing results e.g. \textsc{gal-cols} and \textsc{gal-dens} coincide with the data from the \textsc{bigmdlc} to a high degree. However, \textsc{gal-dens} agrees best with the \textsc{hama} at low halo masses but then coincide with the other two samples at $M_{200c} \sim 10^{13.5} \text{M}_\odot$. In general we expect \textsc{galacticus}' samples not to follow the \textsc{hama} from Behroozi et al. (2013) because they use very different SMF to build-up their model (\textsc{primus} and GALEX Moustakas et al. 2013\footnote{The difference between \textsc{galex} and \textsc{galacticus} can be found in Knebe et al. (2018, fig. 1).}). Their SMF predicts less massive objects than those from \textsc{boss} as we also found for \textsc{gal-dens} sample.

Additionally, we tested the impact on the results using \textsc{galacticus} native definition of overdensities ($\Delta_{\text{NFW}}$) and their corresponding halo mass $M_{200\text{NFW}}$. The impact on the \textsc{shmf} is small but visible on most massive haloes, but within the error estimations.

\subsection{Star formation efficiency}

In the middle panel of Fig. 6 we plot the corresponding $M_*$ at fixed halo mass and show that the stellar masses truly stays constant for increasing halo masses up to $M_{\text{halo}} \sim 10^{13.5} \text{M}_\odot$ considering \textsc{gal-cols} and \textsc{gal-mass}. Then $M_*$ increases continuously which...
Table 2. The table summarizes the median and 1st (subscripted) and 3rd (superscripted) quartile values of various galaxy properties for central galaxies in different environments and mock galaxy samples. Column (i) states the name of the CMASS-mock sample (and population if given). Thereby ‘Pop (A)’ refers to Population (A) and ‘Pop (B)’ to Population (B). Column (ii) indicates the environment (knot or filament) and (iii) their corresponding fraction. Results for the median values of halo mass $M_{200c}$, stellar mass $M_*$, specific star formation rate $sSFR$, gas-phase metallicity $Z_{\text{Cold}}$, cold-gas fraction $M_{\text{Cold}}/M_*$, and black hole mass $M_{\text{BH}}$, respectively, are given in columns (iv)–(ix). Note that we only analysed galaxies in knots and filaments if their number of objects is significantly high, otherwise results for the whole sample is given as for Gal-cols.

| Sample name and population | Environment | Fraction of galaxies | log$_{10}(M_{200c}$ [M$_\odot$]) | log$_{10}(M_*$ [M$_\odot$]) | log$_{10}$(sSFR [yr$^{-1}$]) | $Z_{\text{Cold}}$ | log$_{10}(M_{\text{Cold}}/M_*)$ | log$_{10}(M_{\text{BH}}$ [M$_\odot$]) |
|---------------------------|-------------|----------------------|-----------------------------------|-------------------------------|-----------------------------|----------------|--------------------------------|----------------------------------|
| Gal-cols                  | knot        | 0.61                 | 13.79$^{+0.21}_{-0.19}$           | 11.44$^{+0.11}_{-0.09}$       | $-11.77^{+0.35}_{-0.37}$    | 9.10$^{+0.18}_{-0.16}$   | $-1.14^{+0.20}_{-0.26}$       | 8.65$^{+0.21}_{-0.19}$           |
| Gal-cols                  | filament    | 0.37                 | 13.57$^{+0.19}_{-0.17}$           | 11.37$^{+0.09}_{-0.05}$       | $-11.52^{+0.30}_{-0.34}$    | 9.18$^{+0.21}_{-0.17}$   | $-1.25^{+0.22}_{-0.30}$       | 8.53$^{+0.19}_{-0.16}$           |
| Gal-dens                  | knot        | 0.52                 | 13.55$^{+0.27}_{-0.28}$           | 11.28$^{+0.15}_{-0.14}$       | $-11.53^{+0.36}_{-0.42}$    | 9.25$^{+0.36}_{-0.23}$   | $-1.35^{+0.31}_{-0.65}$       | 8.43$^{+0.26}_{-0.26}$           |
| Gal-dens                  | filament    | 0.41                 | 13.22$^{+0.23}_{-0.26}$           | 11.14$^{+0.13}_{-0.14}$       | $-11.36^{+0.32}_{-0.44}$    | 9.52$^{+0.30}_{-0.35}$   | $-1.83^{+0.54}_{-0.77}$       | 8.20$^{+0.25}_{-0.24}$           |
| Gal-dens Pop(A)           | knot        | 0.26                 | 13.13$^{+0.32}_{-0.34}$           | 11.05$^{+0.07}_{-0.09}$       | $-11.40^{+0.38}_{-0.53}$    | 9.76$^{+0.19}_{-0.29}$   | $-2.32^{+0.61}_{-0.71}$       | 8.05$^{+0.19}_{-0.17}$           |
| Gal-dens Pop(A)           | filament    | 0.62                 | 13.01$^{+0.22}_{-0.22}$           | 11.02$^{+0.08}_{-0.11}$       | $-11.40^{+0.39}_{-0.58}$    | 9.80$^{+0.19}_{-0.25}$   | $-2.42^{+0.57}_{-0.74}$       | 8.00$^{+0.17}_{-0.16}$           |
| Gal-dens Pop(B)           | knot        | 0.54                 | 13.69$^{+0.23}_{-0.21}$           | 11.36$^{+0.13}_{-0.13}$       | $-11.58^{+0.35}_{-0.40}$    | 9.13$^{+0.17}_{-0.17}$   | $-1.18^{+0.21}_{-0.31}$       | 8.56$^{+0.22}_{-0.20}$           |
| Gal-dens Pop(B)           | filament    | 0.44                 | 13.46$^{+0.18}_{-0.16}$           | 11.29$^{+0.09}_{-0.07}$       | $-11.33^{+0.26}_{-0.32}$    | 9.23$^{+0.23}_{-0.19}$   | $-1.33^{+0.26}_{-0.34}$       | 8.42$^{+0.20}_{-0.16}$           |

(i) (ii) (iii) (iv) (v) (vi) (vii) (viii) (ix)

**Figure 6.** Top: SHMF of central galaxies of GALACTICUS’ CMASS-mock samples: Gal-cols (blue solid line), Gal-dens (red dashed line), and Gal-mass (grey dotted–dashed line). They are in excellent agreement with BiGMD-LC within 0.5 < z < 0.6 (filled yellow circles), various HAMs realizations at z ~ 0.55 (shown as a thin green line) from Behroozi et al. (2013), and weak-lensing observation from CFHT Stripe 82 (0.4 < z < 0.6) from Shan et al. (2017) (shaded yellow area). The additional right y-axis represents the estimated halo concentration parameter $C_{\text{NFW}}$ for Gal-cols and Gal-dens, respectively. Middle and Bottom: Stellar masses, $M_*$, and values for the intrinsic scatter, $\sigma_{\log_10(M_*)}$, respectively, as a function of $M_{200c}$ for the same samples as shown in the top panel.
explains the shallower slope of the \textit{SHMF} in the high-mass regime. That means that the most massive haloes in the CMASS-mock host galaxies which have been producing stars more efficiently in their lifetime compared to the BigMD-LC or the HAM.

### 5.1.3 Intrinsic scatter $\sigma_{\log\,M_*}$

In the lower panel of Fig. 6 we plot the intrinsic scatter between stellar and halo mass, $\sigma_{\log\,M_*}$, for GALACTICUS CMASS-mock samples. As reported in the literature (e.g. Moster et al. 2010; Leauthaud et al. 2011; More et al. 2010; Tinker et al. 2017), the relation between the stellar and halo mass is not one-to-one, meaning that the most massive haloes do not host the most massive galaxies (as requested by e.g. HAM models). Furthermore, two haloes with the same mass can host different galaxies with different stellar masses due to distinct assembly history, environmental effects, or feedback mechanisms (to name only a few). The distribution in stellar mass at fixed halo mass is called ‘intrinsic (lognormal) scatter’ and is given by the standard deviation of logarithmic base 10 stellar mass at that halo mass (Tinker et al. 2013). As shown in the lower panel of Fig. 6, $\sigma_{\log\,M_*}$ varies from sample to sample. It depends strongly on halo mass for Gal-cols and Gal-mass and drops to a minimum at $M_{200c} \sim 10^{13} M_\odot$. This means that for growing halo mass, the stellar mass of galaxies residing in these haloes stays constant until the halo reaches a certain mass threshold. Gal-dens does not exhibit such a threshold or minimum, but shows an almost constant scatter of $\sigma_{\log\,M_*} \approx 0.15$ dex for haloes with masses of $M_{200c} > 10^{14} M_\odot$ and then declines smoothly to $\sigma_{\log\,M_*} = 0.09$ dex for $M_{200c} < 10^{14} M_\odot$. Due to the down-sampling process on the SMF of BOSS, Gal-dens exhibits a higher fraction of low-mass haloes than the other CMASS-mocks which is reflected in the intrinsic scatter.

### 5.1.4 Halo occupation distribution

As a second tool to describe galaxy–halo connection, we present the HOD, the mean number of galaxies per halo, $<N_{\text{halo}}>$, as a function of the halo mass, $M_{200c}$. The contribution to the form of the HOD can be divided into central galaxies, modelled as a step function, and satellites, following a power law (Berlind et al. 2003; Zheng et al. 2005). In Fig. 7 we show in three panels the HOD components for our CMASS-mocks from left to right: Gal-cols, Gal-dens, and Gal-mass.

Furthermore, we compare to an HOD-fit from \textit{N}-body simulations constructed from SDSS-III DR10 data (Reid et al. 2014, their MEDRES0 simulation box) modified to the number density of CMASS at $z = 0.56$ (by applying a factor of $1/1.31$ to their HOD in order to correct from their adopted number density to $n = 1.02 \times 10^{-4} \text{Mpc}^{-3}$). We use their best-fitting model from an adaptation of Zheng et al. (2005). We further compare to the first MDPL cosmological simulation. This simulation uses the same cosmology and parameters as MDPL2, like $1 h^{-1}\text{Gpc}$ side-length of the box and we constructed the HODs by applying the same HAM-recipe as described in Rodríguez-Torres et al. (2016) for the BigMDPL.

All GALACTICUS CMASS-mock samples show highly diverse shapes of their HODs where the Gal-dens follows our adopted reference best. In the high-mass end and for the contribution of satellites, Gal-dens agrees with the observations better than the other two. Although Gal-cols and Gal-mass show abundances of satellites in agreement with observations ($\sim 10$ per cent, see Table 1), Gal-dens is with 15 per cent satellites, the only sample where the HOD of satellites is comparable to the data.

The ‘knees’\textsuperscript{14} of the HOD differ a lot between the CMASS-mock sample being estimated by eyeballing: $M_{\text{halo}} \sim 10^{13.7} M_\odot$ for Gal-cols and $M_{\text{halo}} \sim 10^{13.5} M_\odot$ for Gal-dens and Gal-mass, respectively, and to the observation with $M_{\text{min}} \approx 10^{13.180} M_\odot$. The transition between a halo hosting zero to at least one galaxy is more gradually for Gal-dens and more steep for Gal-cols and Gal-mass. The halo mass where a halo cannot host at least one satellite anymore (see short dashed line) varies from $M_{\text{halo}} \sim 10^{13.3} M_\odot$ (Gal-dens) to $M_{\text{halo}} \sim 10^{13.5} M_\odot$ (Gal-cols) and corresponds to $M_{\text{sat}} = 10^{13.328} M_\odot$ for the observations and BigMD-LC, respectively.

All CMASS-mock samples show a similar $M_{200c} M_1$ in the range $10^{14.3} < M_{200c} < 10^{14.7} M_\odot$ compared to the data with $M_{200c} \sim 10^{14.2} M_\odot$. A large plateau also corresponds to large $M_1/M_{\text{min}}$ ratio being $\sim 10$ for Gal-cols and Gal-mass and $\sim 6$ for Gal-dens, compared to our references with $\sim 11$. This ratio has a significant impact on the shape of the correlation function (Benson et al. 2000) meaning that galaxies within a wide range of mass or luminosity exhibit power-law correlation functions (Zheng et al. 2005).

The HODs for centrals (blue thick dashed lines) show incompleteness at the highest halo mass for all GALACTICUS CMASS-mocks, mainly due to the limited volume of the simulation box. We also see that the Gal-dens CMASS-mocks lacks significantly in high-mass central galaxies which have been excluded during the down-sampling procedure. However, the abundance of the satellites are in complete agreement with our references. Furthermore, the fact that Gal-cols and Gal-mass show a smaller scatter in stellar mass than Gal-dens can be directly read from the HODs of the satellites.

### 5.2 TWO-POINT CORRELATION FUNCTION (2pCF)

In this section we present our results for the projected two-point correlation function (2pCF) for our CMASS-mock samples. We use the CORRFUNC software package\textsuperscript{16} from Sinha (2016) and the standard Landy & Szalay (1993) estimator to calculate the functions. We produce 2pCFs with 20 log-spaced bins in the range of $0.5 < r_p < 150 \text{ Mpc}$ with an integration length of $\pi_{\text{max}} = 150 \text{ Mpc}$. We also show the influence of the galaxy type by calculating correlation functions for central and satellite galaxies (short: centrals + sat) and centrals only.

#### 5.2.1 2pCFs for different galaxy types

In Fig. 8 we present 2pCFs for centrals and satellite galaxies (left) and centrals only (right). We compare to the BigMD-LC\textsuperscript{17} within $0.5 < z < 0.6$ using the same data and treatment as described in Rodríguez-Torres et al. (2016, section 5.1). We estimate the uncertainties of our CMASS-mocks for centrals and satellites using 200 realizations of the MD-PATCHY mocks Kitaura et al. (2016). In order to account for the smaller box size-length of MDPL2 we used

\textsuperscript{14}The probability that half of the haloes host at least one galaxy, equal to $M_{\text{min}}$.

\textsuperscript{15}The probability to find one satellite/halo drops to $< 1$ (equal to $M_1$).

\textsuperscript{16}http://corrfunc.readthedocs.io/en/master/index.html

\textsuperscript{17}Note that we do not compare directly with observations because Rodríguez-Torres et al. (2016) already showed that the BigMD-LC agrees very well with BOSS (see their fig. 10). Therefore, we treat BigMD-LC data like observations in this work. Furthermore, we calculated the BigMD-LC data points using a rescaled light-cone to match the box size of MULTI DARK.
Figure 7. HODs split into their components where solid lines represent centrals + satellite galaxies (short: centrals + sats), long dashed lines represent centrals, and short dashed lines represent satellites only. GALACTICUS’ samples are shown as thick blue lines in the panels from left to right: Gal-cols, Gal-dens, and Gal-mass. We compare to the HOD model from Reid et al. (2014) (thin red lines) and to the BIGMD-LC based on abundance matching from Rodríguez-Torres et al. (2016) (yellow filled circles on black thin lines) using the same line style keys as GALACTICUS for their HOD components. \( <N_{\text{gal}} > \) is the mean number of galaxies of a halo with a certain mass \( M_{200c} \).

Figure 8. The projected two-point correlation function for GALACTICUS CMASS-mock samples: Gal-cols (blue solid line), Gal-dens (red dashed line), and Gal-mass (grey dotted–dashed line) at redshift \( z = 0.56 \) compared to the BIGMD-LC (filled yellow circles) for centrals + sats (left) and centrals only (right). The amplitude and shape of the 2pCF is highly diverse for our different CMASS-mock samples and also depends on the galaxy type. The best reproduction of the observations was achieved in general by the Gal-cols sample.

the MD-PATCHY mocks down-scaled to \( 1 \, h^{-1} \) Gpc. We note that we did not construct error bars for centrals only because the MD-Patchy code does not distinguish between central and satellites.

In the lower panel of Fig. 8, we show the residuals for GALACTICUS CMASS-mock samples compared to the BIGMD-LC. The CMASS-mocks Gal-cols and Gal-mass fail to reproduce the 2pCF of the BIGMD-LC, independently if considering centrals and satellite galaxies together or centrals only. However, the shape of their functions are similar but they exhibit a constant shift of \( \sim 0.5 \) dex towards higher amplitudes compared to BIGMD-LC. Only Gal-dens is in very good agreement with the data over a large range of \( r_p \) for both, centrals and satellites and centrals only.

If we include low-mass objects as in the Gal-dens sample the clustering amplitude is reduced at all scales except of the largest with \( r_p > 40 \) Mpc in full agreement with the results of the the HODs in Fig. 7. The left-hand panel of that figure shows that low-mass haloes are underrepresented in the Gal-cols’ HODs resulting in a higher amplitude of the correlation functions in Fig. 8, because only the distances between the most massive objects have been taken into account. Gal-dens’ HOD (middle panel) and 2pCF agree well with both, MD-LC in Fig. 7 and BIGMD-LC in Fig. 8, because more low-mass objects could enter the sample. This is true for centrals and satellite galaxies or for centrals only. We therefore investigate which galaxies contribute the most to the correlation function by selecting subsamples for different subsequent stellar mass cuts. We further hereafter drop the discussion of the Gal-mass sample because the results from it is almost identical to that from the Gal-cols sample.

5.2.2 2pCFs of various subsequent \( M_\star \) cuts

We show the 2pCFs of subsamples of the CMASS-mock sample Gal-dens in Fig. 9. The subsamples were constructed by applying a subsequent stellar masses cuts in \( \log_{10}(M_\star / M_\odot) \): (cut1) 11.21, (cut2) 11.31, (cut3) 11.41, (cut4) 11.51, and (cut5) 11.61. We use again 200 realizations of the MD-PATCHY mocks for the estimation.
of the uncertainties as in Fig. 8. Note that we only present results for Gal-dens because only this sample provides a sufficient number density of galaxies. We can see in the figure that modelled and observed galaxies are in poor agreement with each other. In order to improve the clustering we tried to fix the number density \( n \) of GALACTICUS' subsamples in order to match those of BOSS-CMASS DR12. This experiment only improved the 2pCF slightly.

6 DISCUSSION

Before we discuss our results we want to add a few notes about the influence of GALACTICUS native tuning and model configuration. Most importantly, GALACTICUS has not been specifically calibrated on MDPL2, but its most favourable parameter set and configuration were used. Although GALACTICUS was tuned to match the \( K \), \( b_J \)-band LFs at \( z = 0 \) and the local CMD at \( z = 0.1 \), its luminosities and colours do not perfectly match the CMASS galaxy properties. Therefore, we examine if alternative approaches to select a CMASS-mock (e.g. a cut in stellar mass) would be a convenient approach. Therefore, we examine if alternative approaches to select a CMASS-mock (e.g. a cut in stellar mass) would be a convenient approach.

Why does a density-selected sample work better? First, Gal-dens exhibits by construction the same number density as CMASS. Secondly, although Gal-dens' galaxies are 1.5–2 mag fainter in the \( i \)-band than Gal-cols, Gal-mass, and CMASS (as shown in the upper panel of Fig. 3), their stellar masses are fully comparable\(^\text{18}\) and should have satisfied the CMASS colour–magnitude selection criteria, but due to their lower brightness they did not enter the sample selection.

What are the properties of Gal-dens galaxies? We can divide Gal-dens into two distinct populations (A) and (B) using a sliding cut in SFR depending on sSFR.\(^\text{19}\) Population (A) galaxies are low star forming (SFR \( \sim 0.05 M_\odot \text{yr}^{-1} \)) and live in low-mass haloes \( (M_{200} < 10^{13} M_\odot) \) while Population (B) are star forming (0.1 < SFR < 0.3 \( M_\odot \text{yr}^{-1} \)) residing in most massive haloes \( (M_{200} > 10^{13.3} M_\odot) \). We find a strong dependency on halo mass at fixed sSFR where low-mass haloes have a linear relation between SFR and sSFR, while the high-mass haloes exhibit larger SFRs at fixed sSFR. Furthermore, certain galaxy properties related to star formation can be clearly mapped on to Population (A) or (B) but other properties such as \( M_* \) or \( (r-i) \) colour are continuously distributed. This trend is particularly interesting because it shows the importance of secondary parameters related to the clustering besides halo mass as suggested by Wang, De Lucia & Weinmann (2013).

How do gas-phase properties divide the sample into two distinct populations? In Fig. 10 we show the gas-phase metallicity \( Z_{\text{Cold}} \), a proxy for gas-cooling and star formation (Lebouteiller et al. 2013), for central galaxies. The two populations (A) and (B) are reflected in the bimodal distribution of \( Z_{\text{Cold}} \) where \( \sim 80 \) per cent of Population (A) shows \( Z_{\text{Cold}} > 9.5 \) and only 20 per cent lower values with \( Z_{\text{Cold}} \sim 9.5 \). The opposite is true for Population (B). Common studies of fundamental relations between metallicity, mass, and star formation suggest that less/more massive galaxies have also lower/higher metal abundances (Lara-López et al. 2009; Yates et al. 2016).

\(^\text{(13)}\) The following conditional equation divides the sample into Population (A) and (B):

\[
\log_{10}(\text{SFR}[M_\odot \text{yr}^{-1}]) \begin{cases} < \delta \quad \text{Pop(A)} \\ \geq \delta \quad \text{Pop(B)} \end{cases}
\]

where \( \delta = \frac{\log_{10}(\text{SFR}[\text{yr}^{-1}]) + 11.16}{1.12} \)

\(^\text{(20)}\) \( Z_{\text{Cold}} = 8.69 + \log_{10}(M_{Z,\text{Cold}}/M_{\odot}) - \log_{10}(Z_\odot) \), where \( M_{Z,\text{Cold}} = \) the mass of metals in the cold gas phase, \( Z_{\text{Cold}} \) is normalized by the metallicity of the Sun \( Z_\odot = 0.0134 \) (Asplund et al. 2009), while the factor 8.69 (Allende Prieto, Lambert & Asplund 2001) corresponds to its oxygen abundance.
Our results show that Population (B)’s galaxies are more massive but have lower metal abundances. This ‘turnover’ was also reported by Yates et al. (2012) for modelled galaxies at $z = 0$ and is possibly linked to the infall of metal-poor gas after a gas-rich merger. In Yates & Kauffmann (2014) the same authors studied massive galaxies and divide them into an ‘enriching’ and a ‘diluting’ sample, the later show similar trends as our Population (B): low sSFR, lower $Z_{\text{Cold}}$, and higher $M_{\text{BH}}$. Furthermore, our findings are in total agreement with Lara-Lopez et al. (2013) showing that galaxies with low sSFR have high/low values of $Z_{\text{Cold}}$ when $M_{\text{Cold}}$ is low/high. We emphasize that the distinct separation of the two populations could give clues about galaxy evolution in the context of the origin of the fundamental luminosity/mass–metallicity relation, merger-induced star formation, or ‘downsizing’ (Mannucci et al. 2010, see their section 1 for comparison).

How do the Populations (A) and (B) relate to environment? We expect that Population (A) fixes the clustering amplitude due to their section 1 for comparison). We detect a clear environmental dependency of this sample where the number fraction of galaxies has significantly smaller halo mass, stellar mass, cold-gas fraction, and black hole mass than Population (B) in both environments. Smaller scatter could mean that there is insufficient scatter in the assembly history, or that the galaxy formation models do not capture all of it. However, understanding this issue is a non-trivial task and one has to address model specific properties in more detail to understand which combination of properties causes this effect. We find that the comparison with other SAMs would help on this task, but would be beyond the scope of this paper and is therefore left for further studies.

7 SUMMARY

Our work is based on the BOSS (Schlegel et al. 2009; Dawson et al. 2013) of the Sloan Digital Sky Survey (SDSS-III, Eisenstein et al. 2011) CMASS (for ‘constant mass’) and a semi-analytical model of galaxy formation (SAM), called GALACTICUS, as part of the MULTIDARK-GALAXIES products (Knebe et al. 2018). The CMASS sample was built from the SDSS-III/BOSS survey catalogues by applying a complex colour–magnitude selection (see equations 1–4). We use the same selection scheme to extract our modelled galaxy catalogue from GALACTICUS, called Gal-coIs, at $z = 0.56$.

We provide detail assessment of the SAM via comparing with BOSS as well as results on the galaxy–halo connection and clustering studies of the two-point correlation function. For reasons stated in Section 3, we construct two additional CMASS-mock samples. The first one is called Gal-dens and was build by randomly selecting modelled galaxies (or down-sampling) until they fit the observational SMF of BOSS in the range $0.5 < z < 0.6$. The second CMASS-mock is called Gal-mass and was generated by applying a high stellar mass cut of $M_*>10^{11.25} M_{\odot}$ as introduced by Maraston et al. (2013). Here we summarize major results of our study.

(i) The GALACTICUS colour–magnitude-selected CMASS-mock sample, Gal-coIs, shows a lower number density, fewer blue objects, and is located within a smaller parameter space compared to the observational sample (see Fig. 1). Its RS is intrinsically concentrated, as predicted by Montero-Dorta et al. (2016) (see Fig. 2). Although the number density of this sample is only 1/3 the density of BOSS galaxies, Gal-coIs overpredicts red galaxies at $M_* > 10^{12} M_{\odot}$ (see Fig. 4). Galaxies in Gal-dens satisfy the
CMASS colour selection criteria, but they did not enter the sample selection due to their luminosities being approximately 1.5–2 mag lower in i-band (see the middle panel of Fig. 3).

(ii) GALACTICUS Gal-cols and Gal-mass samples agree very well with the stellar to halo mass relation of Rodríguez-Torres et al. (2016) and weak-lensing results from Shan et al. (2017), while Gal-dens shows similar behaviour as the HAM model from Behroozi et al. (2013) (see Fig. 6). However, all three CMASS-mock samples exhibit an increasing scatter at fixed halo mass from $\sigma_{\log M_\ast} \sim 0.05$–0.15 dex depending on halo mass. Compared to other works with $\sigma_{\log M_\ast} = 0.14$ dex by Rodríguez-Torres et al. (2016), $\sigma_{\log M_\ast} = 0.18 \pm 0.02$ dex by Tinker et al. (2017), or 0.249 ± 0.019 dex by Leauthaud et al. (2012), GALACTICUS displays an insufficient level of scatter.

(iii) Gal-cols and Gal-mass agree poorly with the clustering of CMASS galaxies from the high-fidelity mock BitMD-LC (Rodríguez-Torres et al. 2016), which was obtained using HAM techniques. We find that the combination of low intrinsic scatter at fixed halo mass and missing objects (or objects being too faint) is responsible for the high clustering amplitudes of Gal-cols and Gal-mass. However, the Gal-dens sample reproduces the clustering of central and satellite galaxies as well as of centrals only, within 1 $\sigma$ (see Fig. 8).

(iv) We can divide the Gal-cols and Gal-dens samples into two subpopulations, (A) and (B), using a given SFR cut. Population (A) corresponds to low star-forming galaxies in lower mass haloes, while Population (B) is comprised of mildly star-forming galaxies living in the most massive haloes. (A)-galaxies were found as the population which displays too faint luminosities as mentioned in (i), but fix the clustering amplitude due to the environmental affiliation and number density. Using the VWEB code (see Appendix A) we confirm that (A)-galaxies live in filaments, while (B)-galaxies can be found in knots.

(v) We find further correlations between halo mass $M_{200\text{c}}$ and star-formation-related properties as (specific) star formation rate, gas-phase metallicity, $Z_{\text{cold}}$, and cold-gas fraction, $M_{\text{cold}}/M_{\ast}$, but also black hole mass $M_{\text{BH}}$, depending on the environment and subpopulation (A) and (B) where e.g. 80 per cent of galaxies in Population (A) show higher sSFR and $Z_{\text{cold}} > 9.5$, but lower cold-gas fractions and black hole masses compared to their counterparts in Population (B) (see Table 2).

In this work, we have carefully examined several samples of the most massive galaxies from the GALACTICUS galaxy formation model. In a follow-up work, we plan to extend this analysis to other SAMs in order to study in more detail the star formation history of massive galaxies at intermediate redshifts. This follow-up study will be connected to the effect of galaxy assembly bias, a crucial aspect to the formation and evolution of galaxies.

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APPENDIX A: THE VWEB METHOD

This Vweb method applies the shear tensor technique to classify the large-scale environments into either ‘void’, ‘sheet’, ‘filament’, or ‘knot’. Following Hoffman et al. (2012), the velocity shear tensor is defined as

$$\Sigma_{\alpha\beta} = -\frac{1}{2H_0} \left( \frac{\partial v_\alpha}{\partial r_\beta} + \frac{\partial v_\beta}{\partial r_\alpha} \right),$$  
(A1)

where, $H_0$ is the Hubble constant. The eigenvalues of $\Sigma_{\alpha\beta}$ are denoted as $\lambda_i$ ($i = 1, 2$ and $3$).

The simulation box is separated into cubic mesh cells, within which the velocity field is calculated. Each cell has a size of $\sim \text{1 Mpc}$. After smoothing the velocity field, we calculate the eigenvalues of the velocity shear tensor in each cell. Each cell is then classified as either ‘void’, ‘sheet’, ‘filament’, or ‘knot’ according to the eigenvalues $\lambda_1 > \lambda_2 > \lambda_3$:

1. void, if $\lambda_1 < \lambda_{th}$,
2. sheet, if $\lambda_1 \geq \lambda_{th} > \lambda_2$,
3. filament, if $\lambda_2 \geq \lambda_{th} > \lambda_3$,
4. knot, if $\lambda_3 \geq \lambda_{th}$,

where $\lambda_{th}$ is a free threshold parameter (Hoffman et al. 2012; Libeskind et al. 2012, 2013). Following the discussion of Carlesi et al. (2014); Cui et al. (2018, 2019), we set $\lambda_{th} = 0.1$, which presents better agreement to the visualized density field. Our mock galaxies are then placed on to the same grid checking for the web classification of the cell they lie in.

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