A Kernel PCA Method for Superior Word Sense Disambiguation

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Abstract

We introduce a new method for disambiguating word senses that exploits a nonlinear Kernel Principal Component Analysis (KPCA) technique to achieve accuracy superior to the best published individual models. We present empirical results demonstrating significantly better accuracy compared to the state-of-the-art achieved by either naïve Bayes or maximum entropy models, on Senseval-2 data. We also contrast against another type of kernel method, the support vector machine (SVM) model, and show that our KPCA-based model outperforms the SVM-based model. It is hoped that these highly encouraging first results on KPCA for natural language processing tasks will inspire further development of these directions.

1 Introduction

Achieving higher precision in supervised word sense disambiguation (WSD) tasks without resorting to ad hoc voting or similar ensemble techniques has become somewhat daunting in recent years, given the challenging benchmarks set by naïve Bayes models (e.g., Mooney (1996), Chodorow et al. (1999), Pedersen (2001), Yarowsky and Florian (2002)) as well as maximum entropy models (e.g., Dang and Palmer (2002), Klein and Manning (2002)). A good foundation for comparative studies has been established by the Senseval data and evaluations; of particular relevance here are the lexical sample tasks from Senseval-1 (Kilgarriff and Rosenzweig, 1999) and Senseval-2 (Kilgarriff, 2001).

We therefore chose this problem to introduce an efficient and accurate new word sense disambiguation approach that exploits a nonlinear Kernel PCA technique to make predictions implicitly based on generalizations over feature combinations. The technique is applicable whenever vector representations of a disambiguation task can be generated; thus many properties of our technique can be expected to be highly attractive from the standpoint of natural language processing in general.

In the following sections, we first analyze the potential of nonlinear principal components with respect to the task of disambiguating word senses. Based on this, we describe a full model for WSD built on KPCA. We then discuss experimental results confirming that this model outperforms state-of-the-art published models for Senseval-related lexical sample tasks as represented by (1) naïve Bayes models, as well as (2) maximum entropy models. We then consider whether other kernel methods—in particular, the popular SVM model—are equally competitive, and discover experimentally that KPCA achieves higher accuracy than the SVM model.

2 Nonlinear principal components and WSD

The Kernel Principal Component Analysis technique, or KPCA, is a nonlinear kernel method for extraction of nonlinear principal components from vector sets in which, conceptually, the n-dimensional input vectors are nonlinearly mapped from their original space $\mathbb{R}^n$ to a high-dimensional feature space $F$ where linear PCA is performed, yielding a transform by which the input vectors can be mapped nonlinearly to a new set of vectors (Schölkopf et al., 1998).

A major advantage of KPCA is that, unlike other common analysis techniques, as with other kernel methods it inherently takes combinations of predictive features into account when optimizing dimensionality reduction. For natural language problems in general, of course, it is widely recognized that significant accuracy gains can often be achieved by generalizing over relevant feature combinations (e.g., Kudo and Matsumoto (2003)). Another advantage of KPCA for the WSD task is that the dimensionality of the input data is generally very

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large, a condition where kernel methods excel.

*Nonlinear principal components* (Diamantaras and Kung, 1996) may be defined as follows. Suppose we are given a training set of $M$ pairs $(x_t, c_t)$ where the observed vectors $x_t \in \mathbb{R}^n$ in an $n$-dimensional input space $X$ represent the context of the target word being disambiguated, and the correct class $c_t$ represents the sense of the word, for $t = 1, ..., M$. Suppose $\Phi$ is a nonlinear mapping from the input space $\mathbb{R}^n$ to the feature space $F$. Without loss of generality we assume the $M$ vectors are centered vectors in the feature space, i.e., $\sum_{t=1}^M \Phi(x_t) = 0$; uncentered vectors can easily be converted to centered vectors (Schölkopf et al., 1998). We wish to diagonalize the covariance matrix in $F$:

$$C = \frac{1}{M} \sum_{j=1}^M \Phi(x_j) \Phi^T(x_j) \quad (1)$$

To do this requires solving the equation $\lambda v = Cv$ for eigenvalues $\lambda \geq 0$ and eigenvectors $v \in F$. Because

$$Cv = \frac{1}{M} \sum_{j=1}^M (\Phi(x_j) \cdot v) \Phi(x_j) \quad (2)$$

we can derive the following two useful results. First,

$$\lambda (\Phi(x_t) \cdot v) = \Phi(x_t) \cdot Cv \quad (3)$$

for $t = 1, ..., M$. Second, there exist $\alpha_i$ for $i = 1, ..., M$ such that

$$v = \sum_{i=1}^M \alpha_i \Phi(x_i) \quad (4)$$

Combining (1), (3), and (4), we obtain

$$M \lambda \sum_{i=1}^M \alpha_i (\Phi(x_t) \cdot \Phi(x_i))$$

$$= \sum_{i=1}^M \alpha_i (\Phi(x_t) \cdot \sum_{j=1}^M \Phi(x_j)) (\Phi(x_j) \cdot \Phi(x_i))$$

for $t = 1, ..., M$. Let $\hat{K}$ be the $M \times M$ matrix such that

$$\hat{K}_{ij} = \Phi(x_t) \cdot \Phi(x_j) \quad (5)$$

and let $\hat{\lambda}_1 \geq \hat{\lambda}_2 \geq \ldots \geq \hat{\lambda}_M$ denote the eigenvalues of $\hat{K}$ and $\hat{\alpha}^1, ..., \hat{\alpha}^M$ denote the corresponding complete set of normalized eigenvectors, such that $\hat{\lambda}_t (\hat{\alpha}^t \cdot \hat{\alpha}^t) = 1$ when $\hat{\lambda}_t > 0$. Then the $l$th nonlinear principal component of any test vector $x_t$ is defined as

$$y^l_t = \sum_{i=1}^M \hat{\alpha}^l_i (\Phi(x_t) \cdot \Phi(x_i)) \quad (6)$$

where $\hat{\alpha}^l_i$ is the $l$th element of $\hat{\alpha}^l$.

To illustrate the potential of nonlinear principal components for WSD, consider a simplified disambiguation example for the ambiguous target word “art”, with the two senses shown in Table 1. Assume a training corpus of the eight sentences as shown in Table 2, adapted from Senseval-2 English lexical sample corpus. For each sentence, we show the feature set associated with that occurrence of “art” and the correct sense class. These eight occurrences of “art” can be transformed to a binary vector representation containing one dimension for each feature, as shown in Table 3.

Extracting nonlinear principal components for the vectors in this simple corpus results in nonlinear generalization, reflecting an implicit consideration of combinations of features. Table 3 shows the first three dimensions of the principal component vectors obtained by transforming each of the eight training vectors $x_t$ into (a) principal component vectors $z_t$ using the linear transform obtained via PCA, and (b) nonlinear principal component vectors $y_t$ using the nonlinear transform obtained via KPCA as described below.

Similarly, for the test vector $x_g$, Table 4 shows the first three dimensions of the principal component vectors obtained by transforming it into (a) a principal component vector $z_0$ using the linear PCA transform obtained from training, and (b) a nonlinear principal component vector $y_0$ using the nonlinear KPCA transform obtained obtained from training. The vector similarities in the KPCA-transformed space can be quite different from those in the PCA-transformed space. This causes the KPCA-based model to be able to make the correct class prediction, whereas the PCA-based model makes the
Table 2: A tiny corpus for the target word “art”, adapted from the Senseval-2 English lexical sample corpus (Kilgarriff 2001), together with a tiny example set of features. The training and testing examples can be represented as a set of binary vectors: each row shows the correct class c for an observed vector x of five dimensions.

| TRAINING | design/N | media/N | the/DT | entertainment/N | world/N | Class |
|----------|----------|---------|--------|-----------------|---------|-------|
| $x_1$    | He studies art in London.                         |        |        |                  |         | 1     |
| $x_2$    | Punch's weekly guide to the world of the arts, entertainment, media and more. | 1       | 1       | 1                | 1       | 1     |
| $x_3$    | All such studies have influenced every form of art, design, and entertainment in some way. | 1       |        | 1                |         | 1     |
| $x_4$    | Among the technical arts cultivated in some continental schools that began to affect England soon after the Norman Conquest were those of measurement and calculation. |        | 1       |                  | 2       |       |
| $x_5$    | The Art of Love.                                   | 1       |        |                  |         | 2     |
| $x_6$    | Indeed, the art of doctoring does contribute to better health results and discourages unwarranted malpractice litigation. | 1       |        |                  | 2       |       |
| $x_7$    | Countless books and classes teach the art of asserting oneself. | 1       |        |                  |         | 2     |
| $x_8$    | Pop art is an example.                             |        |        |                  |         | 1     |

| TESTING  | design/N | media/N | the/DT | entertainment/N | world/N | Class |
|----------|----------|---------|--------|-----------------|---------|-------|
| $x_9$    | In the world of design arts particularly, this led to appointments made for political rather than academic reasons. | 1       | 1       | 1                | 1       |       |

Wrong class prediction.

What permits KPCA to apply stronger generalization biases is its implicit consideration of combinations of feature information in the data distribution from the high-dimensional training vectors. In this simplified illustrative example, there are just five input dimensions; the effect is stronger in more realistic high dimensional vector spaces. Since the KPCA transform is computed from unsupervised training vector data, and extracts generalizations that are subsequently utilized during supervised classification, it is quite possible to combine large amounts of unsupervised data with reasonable smaller amounts of supervised data.

It can be instructive to attempt to interpret this example graphically, as follows, even though the interpretation in three dimensions is severely limiting. Figure 1(a) depicts the eight original observed training vectors $x_1$ in the first three of the five dimensions; note that among these eight vectors, there happen to be only four unique points when restricting our view to these three dimensions. Ordinary linear PCA can be straightforwardly seen as projecting the original points onto the principal axis,
as can be seen for the case of the first principal axis in Figure 1(b). Note that in this space, the sense 2 instances are surrounded by sense 1 instances. We can traverse each of the projections onto the principal axis in linear order, simply by visiting each of the first principal components $z_1^t$ along the principle axis in order of their values, i.e., such that

$$z_1^t \leq z_3^t \leq z_4^t \leq z_5^t \leq z_6^t \leq z_7^t \leq z_2^t \leq z_3^t \leq z_0$$

It is significantly more difficult to visualize the nonlinear principal components case, however. Note that in general, there may not exist any principal axis in $X$, since an inverse mapping from $F$ may not exist. If we attempt to follow the same procedure to traverse each of the projections onto the first principal axis as in the case of linear PCA, by considering each of the first principal components $y_1^t$ in order of their values, i.e., such that

$$y_1^t \leq y_2^t \leq y_3^t \leq y_4^t \leq y_5^t \leq y_6^t \leq y_7^t \leq y_8^t \leq y_3^t \leq y_2^t$$

then we must arbitrarily select a “quasi-projection” direction for each $y_1^t$ since there is no actual principal axis toward which to project. This results in a “quasi-axis” roughly as shown in Figure 1(c) which, though not precisely accurate, provides some idea as to how the nonlinear generalization capability allows the data points to be grouped by principal components reflecting nonlinear patterns in the data distribution, in ways that linear PCA cannot do. Note that in this space, the sense 1 instances are already better separated from sense 2 data points. Moreover, unlike linear PCA, there may be up to $M$ of the “quasi-axes”, which may number far more than five. Such effects can become pronounced in the high dimensional spaces are actually used for real word sense disambiguation tasks.

### 3 A KPCA-based WSD model

To extract nonlinear principal components efficiently, note that in both Equations (5) and (6) the explicit form of $\Phi(x_i)$ is required only in the form of $(\Phi(x_i) \cdot \Phi(x_j))$, i.e., the dot product of vectors in $F$. This means that we can calculate the nonlinear principal components by substituting a kernel function $k(x_i, x_j)$ for $(\Phi(x_i) \cdot \Phi(x_j))$ in Equations (5) and (6) without knowing the mapping $\Phi$ explicitly; instead, the mapping $\Phi$ is implicitly defined by the kernel function. It is always possible to construct a mapping into a space where $k$ acts as a dot product so long as $k$ is a continuous kernel of a positive integral operator (Schölkopf et al., 1998).
Table 5: Experimental results showing that the KPCA-based model performs significantly better than naïve Bayes and maximum entropy models. Significance intervals are computed via bootstrap resampling.

| WSD Model          | Accuracy | Sig. Int. |
|--------------------|----------|-----------|
| naïve Bayes        | 63.3%    | +/-0.91%  |
| maximum entropy    | 63.8%    | +/-0.79%  |
| KPCA-based model   | 65.8%    | +/-0.79%  |

Thus we train the KPCA model using the following algorithm:

1. Compute an $M \times M$ matrix $\hat{K}$ such that
   \[
   \hat{K}_{ij} = k(x_i, x_j)
   \]

2. Compute the eigenvalues and eigenvectors of matrix $\hat{K}$ and normalize the eigenvectors. Let $\hat{\lambda}_1 \geq \hat{\lambda}_2 \geq \ldots \geq \hat{\lambda}_M$ denote the eigenvalues and $\hat{\alpha}^1, \ldots, \hat{\alpha}^M$ denote the corresponding complete set of normalized eigenvectors.

To obtain the sense predictions for test instances, we need only transform the corresponding vectors using the trained KPCA model and classify the resultant vectors using nearest neighbors. For a given test instance vector $x$, its $l$th nonlinear principal component is

\[
y^l_t = \sum_{i=1}^{M} \hat{\alpha}^l_i k(x_i, x_t)
\]

where $\hat{\alpha}^l_i$ is the $i$th element of $\hat{\alpha}^l$.

For our disambiguation experiments we employ a polynomial kernel function of the form $k(x_i, x_j) = (x_i \cdot x_j)^d$, although other kernel functions such as gaussians could be used as well. Note that the degenerate case of $d = 1$ yields the dot product kernel $k(x_i, x_j) = (x_i \cdot x_j)$ which covers linear PCA as a special case, which may explain why KPCA always outperforms PCA.

4 Experiments

4.1 KPCA versus naïve Bayes and maximum entropy models

We established two baseline models to represent the state-of-the-art for individual WSD models: (1) naïve Bayes, and (2) maximum entropy models. The naïve Bayes model was found to be the most accurate classifier in a comparative study using a
subset of Senseval-2 English lexical sample data by Yarowsky and Florian (2002). However, the maximum entropy (Jaynes, 1978) was found to yield higher accuracy than naïve Bayes in a subsequent comparison by Klein and Manning (2002), who used a different subset of either Senseval-1 or Senseval-2 English lexical sample data. To control for data variation, we built and tuned models of both kinds. Note that our objective in these experiments is to understand the performance and characteristics of KPCA relative to other individual methods. It is not our objective here to compare against voting or other ensemble methods which, though known to be useful in practice (e.g., Yarowsky et al. (2001)), would not add to our understanding.

To compare as evenly as possible, we employed features approximating those of the “feature-enhanced naïve Bayes model” of Yarowsky and Florian (2002), which included position-sensitive, syntactic, and local collocational features. The models in the comparative study by Klein and Manning (2002) did not include such features, and so, again for consistency of comparison, we experimentally verified that our maximum entropy model (a) consistently yielded higher scores than when the features were not used, and (b) consistently yielded higher scores than naïve Bayes using the same features, in agreement with Klein and Manning (2002). We also verified the maximum entropy results against several different implementations, using various smoothing criteria, to ensure that the comparison was even.

Evaluation was done on the Senseval 2 English lexical sample task. It includes 73 target words, among which nouns, adjectives, adverbs and verbs. For each word, training and test instances tagged with WordNet senses are provided. There are an average of 7.8 senses per target word type. On average 109 training instances per target word are available. Note that we used the set of sense classes from Senseval’s “fine-grained” rather than “coarse-grained” classification task.

The KPCA-based model achieves the highest accuracy, as shown in Table 5, followed by the maximum entropy model, with naïve Bayes doing the poorest. Bear in mind that all of these models are significantly more accurate than any of the other reported models on Senseval. “Accuracy” here refers to both precision and recall since disambiguation of all target words in the test set is attempted. Results are statistically significant at the 0.10 level, using bootstrap resampling (Efron and Tibshirani, 1993); moreover, we consistently witnessed the same level of accuracy gains from the KPCA-based model over many variations of the experiments.

4.2 KPCA versus SVM models
Support vector machines (e.g., Vapnik (1995), Joachims (1998)) are a different kind of kernel method that, unlike KPCA methods, have already gained high popularity for NLP applications (e.g., Takamura and Matsumoto (2001), Isozaki and Kazawa (2002), Mayfield et al. (2003)) including the word sense disambiguation task (e.g., Cabezas et al. (2001)). Given that SVM and KPCA are both kernel methods, we are frequently asked whether SVM-based WSD could achieve similar results.

To explore this question, we trained and tuned an SVM model, providing the same rich set of features and also varying the feature representations to optimize for SVM biases. As shown in Table 6, the highest-achieving SVM model is also able to obtain higher accuracies than the naïve Bayes and maximum entropy models. However, in all our experiments the KPCA-based model consistently outperforms the SVM model (though the margin falls within the statistical significance interval as computed by bootstrap resampling for this single experiment). The difference in KPCA and SVM performance is not surprising given that, aside from the use of kernels, the two models share little structural resemblance.

4.3 Running times
Training and testing times for the various model implementations are given in Table 7, as reported by the Unix time command. Implementations of all models are in C++, but the level of optimization is not controlled. For example, no attempt was made to reduce the training time for naïve Bayes, or to reduce the testing time for the KPCA-based model. Nevertheless, we can note that in the operating range of the Senseval lexical sample task, the running times of the KPCA-based model are roughly within the same order of magnitude as for naïve Bayes or maximum entropy. On the other hand, training is much faster than the alternative kernel method based on SVMs. However, the KPCA-based model’s times could be expected to suffer in situations where significantly larger amounts of
training data are available.

5 Conclusion

This work represents, to the best of our knowledge, the first application of Kernel PCA to a true natural language processing task. We have shown that a KPCA-based model can significantly outperform state-of-the-art results from both naïve Bayes as well as maximum entropy models, for supervised word sense disambiguation. The fact that our KPCA-based model outperforms the SVM-based model indicates that kernel methods other than SVMs deserve more attention. Given the theoretical advantages of KPCA, it is our hope that this work will encourage broader recognition, and further exploration, of the potential of KPCA modeling within NLP research.

Given the positive results, we plan next to combine large amounts of unsupervised data with reasonable smaller amounts of supervised data such as the Senseval lexical sample. Earlier we mentioned that one of the promising advantages of KPCA is that it computes the transform purely from unsupervised training vector data. We can thus make use of the vast amounts of cheap unannotated data to augment the model presented in this paper.

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