Elastic properties of single-walled carbon nanotube thin film by nanoindentation test

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This paper carries out a preliminary study for the elastic properties of single walled carbon nanotube (SWCNT) thin film. The SWCNT thin films (~250 nm) are prepared by a simple and cost effective method of spin-coating technology. Nanoindentation test with a Berkovich indenter is used to determine the hardness and elastic modulus of the SWCNT thin film. It is important to note that the elastic properties of SWCNT film are indirectly derived from the information of load and displacement of the indenter under certain assumptions, deviation of the ‘test value’ is inevitable. In this regard, uncertainty analysis is an effective process in guaranty the validity of the material properties. This paper carries out uncertainty estimation for the tested elastic properties of SWCNT film by nanoindentation. Experimental results and uncertainty analysis indicates that nanoindentation test could be an effective and reliable method in determine the elastic properties of SWCNT thin film. Moreover, the obtained values of hardness and elastic modulus can further benefit the design of SWCNT thin film based components.

Exploring the potential of carbon nanotube (CNT) films has been one of the intense researches since the fabrication and purification of thin films of CNTs became a relatively mature technique. The discovery of exceptional transparency, conductivity, and flexibility properties suggest CNT films potential applications in different fields of electronic, optoelectronic, and sensor systems\textsuperscript{1, 2}. Until recently, a lot of work has been done in the fabrication of thin CNT films with optimized collective electrical, optical, and mechanical properties by controlling the tube density, the overall spatial layouts, the lengths, and their orientations\textsuperscript{3}. Wet methods such as drop drying or electrophoretic deposition have been proposed as a convenient method in preparing thin films of CNTs with controlled morphology and desired function\textsuperscript{4, 5}. Compared with the efforts which focused on the techniques for producing well defined CNT films, little attention has been paid to the mechanical properties of these thin films even though the elastic properties could be an important issue in their ultimate application. It is demonstrated that the mechanical deformation of CNTs may cause considerable changes in its electronic, optical, magnetic, and chemical properties\textsuperscript{6, 7}. Besides, the mechanical properties are very different for the CNT films with different chemical component or stress and strain states. Lee found that the poisson’s ratio of SWCNTs and MWNTs sheets can change from 0.06 to −0.20 as the wt% of MWNTs changes from 0 to 100\textsuperscript{8}. Yin and his colleagues discovered that the poisson’s ratio of CNT films can change from negative to positive during a uniaxial tensile loading\textsuperscript{9}. These interest findings indicate that the mechanical properties of CNT films could be essential in fulfilling their ultimate application.

With high-resolution of load and displacement data, nanoindentation test was realized to be a very useful technique in extracting the mechanical properties of materials\textsuperscript{10, 11}. In nanoindentation process, an indenter tip is pressed into the specimen. Penetration and force on the indenter are continuously recorded by high-resolution depth-sensing instruments. The indentation system can reaches a load and displacement resolution of several nN and less than 1 nm, respectively. In addition, nanoindentation does not require the removal of the specimen from its substrate, which greatly reduces the difficulty of specimen preparation. With those properties mentioned above, nanoindentation has been used in determining the mechanical properties of materials in nano/micro-scale and other extracted property in physical sciences\textsuperscript{12}. Qi\textsuperscript{13} used nanoindentation technique and their proposed micro-mechanical model

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to measure the bending stiffness, wall modulus and axial modulus of the constituent nanotubes. Liu\textsuperscript{14} presented an atomistic study on the nanoindentation mechanisms of single-walled and multi-walled CNTs and CNT clusters. Their study demonstrated that the deformation characteristics of CNTs are related to its elastic stiffness.

Those experimental and theoretical studies suggest that nanoindentation technique could be an effective method in determine the mechanical properties of CNT films. As the importance of mechanical properties for SWCNT films in their real applications, the objective of this paper is to investigate the elastic modulus of SWCNT thin film. SWCNT thin films are prepared by using the easy operating and time-saving method of spin-coating technique. The hardness and elastic modulus of SWCNT film are estimated by nanoindentation test. Uncertainty analysis for the tested results indicates that nanoindentation test is a reliable and effective method in determining the elastic properties of SWCNT thin film.

**Experimental Details**

**Material preparation.** In this study, thin SWCNT films are prepared at the mechanical engineering center, University of Coimbra (Portugal) using spin-coating (or drop drying) method, and the spin-coating process is shown in Fig. 1. SWCNTs were prepared by arc discharge technique by the Int’tech Center, Kyoto University in Japan. The average diameter of the SWCNTs is around 1.2 nm. In the process of SWCNT thin films preparation, a dilute suspension of SWCNTs in ethanol was ultrasonicated for 20 min to spread out the nanotubes. The diffused suspension deposited on the well-polished silicon substrates of $1\times10$ mm using spin-coating method. At the beginning of the spin-coating process, a droplet of SWCNT suspension dropped on the substrates, a low spin speed of 200 rpm is used to spread the solution over the substrate, then a relatively high spin speed of 1000 rpm is accelerated to thin the samples to the final desired thickness within the appropriate rotational time, as shown in Fig. 1(b). Ethanol solvent was evaporated at room temperature. The samples were then subjected to heat treatment for 2 h under the temperature of 300 °C and slowly cooled down to room temperature. After heat treatment, nanotubes stuck and randomly oriented on the silicon substrate. The interactions of tube-to-tube and tube-to-substrate are through Van der Waals force. Figure 1(c) and (d) shows the optical microscope images of nanotube clusters distribution on the silicon substrates under 5 times magnification (c) and 50 times magnification (d).

The thickness of the deposited SWCNT film was obtained by a profile-meter technique. The surface profiling was carried out on the film edge. The detection of the scanned edge gives the projected wall thickness. The profile-meter indicates a SWCNTs film thickness of about 250 nm, the width of film is about 0.25 mm.

**Nanoindentation test.** Nanoindentation test measures the movement of a diamond probe in contact with the material surface. For indentation measurements, the indenter is impressed into the material surface under an increasing load; After it reaches a pre-determined maximum load or displacement, the load is reduced and the penetration depth decreasing due to the elastic recovery of the deformed material. Figure 2 shows the cross section of indentation. During indentation process, the displacements versus the applied loads are recorded through

![Figure 1. Spin coating process and the optical microscope images of nanotube clusters distributed on silicon substrates: (a) static dispense process, (b) spin-coating process, (c) microscope images 5×, and (d) microscope images 50×.](image-url)
the precise actuator and sensor. Those records are then used to calculate the indentation hardness and elastic
modules of the tested material. In nanoindentation technique, it is common to define the hardness of the material
as the mean pressure under the load:

\[ H = \frac{P_{\text{max}}}{A} \]  

(1)

where \( P_{\text{max}} \) is the maximum load and \( A \) is the projected contact area at the maximum load which calculated from
the contact depth \( h_c \) \(^{15} \).

\[ A = A(h_c) = 24.5h_c^2 + C_1h_c^{1/2} + C_2h_c^{1/4} + \cdots + C_8h_c^{1/128} \]  

(2)

The Young's modulus is obtained by contact mechanics:

\[ \frac{1}{E_r} = \frac{(1 - \nu^2)}{E} + \frac{(1 - \nu_i^2)}{E_i} \]  

(3)

where \( E \) and \( \nu \) are Young's modulus and Poisson's ratio of the tested material; \( E_i \) and \( \nu_i \) are the same parameters
for the indenter; \( E_r \) is the reduced modulus which can be deduced from the initial slope of the unloading data
(Fig. 3) as:

\[ E_r = \frac{1}{2} \frac{dp}{dh} \frac{\sqrt{\pi}}{\sqrt{A}} \]  

(4)

Experimental tests for SWCNT film were performed at the nanoindentation platform system. The system
has the load and displacement resolution of 1 nN and 0.0002 nm, respectively, the measurement range of film
thickness is more than 200 nm. Berkovich indenter, a three side pyramid with a half angle of 65.3° was used in
the experiment. The test surrounding temperature is controlled within 25 ± 1 °C, the humidity is about 63%. The
test system was placed on a vibration free isolated chamber as shown in Fig. 4. The surface of the specimen is first
scanned, and then a relatively large and uniform area of the film on the substrate was chosen for the test subject
(Fig. 4(c)). The indenter was first loaded and unloaded three times successively at a constant rate to examine the
reversibility of the deformation. Indentations were made at eighteen different nodes on the chosen area. Table 1 is
the parameters setting in indentation procedure.
Experimental Results
Doerner observed that for some materials, the initial portions of unloading curves are linear\(^6\), and the unloading stiffness is then related to the modulus and contact area through the relationship:

\[
S = \frac{dP}{dh} = \frac{2}{\sqrt{\pi}} E_v \sqrt{A}
\]  

(5)

where, \(S = \frac{dP}{dh}\) is the initial unloading stiffness obtained by the initial portion of the unloading process. \(A\) is the projected area of the elastic contact. It is assumed that the contact area between the indenter and the material remains constant and moves elastically during unloading, and the plastic area is always equal to the contact area, and it is calculated using a polynomial function of order 2 in this study.

In this study, the experimental results are corrected for the thermal drift of equipment system. The hardness and elastic modulus are determined by using the method of power law fitting between 100% and 20% of the unloading data.

\[
P = \alpha \left( h - h_j \right)^m
\]  

(6)

where the constant \(\alpha\), \(h_j\), and \(m\) are determined by fitting the upper portion of unloading data. The indentation load-displacement data is analyzed according to equations (1) and (4). The elastic modulus of SWCNT film is then derived from equation (3) as:

\[
E = \left(1 - v^2\right) \left( \frac{1}{E_v} - \frac{1}{E_i} \right)
\]  

(7)

Table 2 represents the averages test results of 18 indentations obtained automatically by the test system. The overview of the experimental results for the 18 groups of load-displacement curves is demonstrated in Fig. 5. And the Reduced modulus vs Maximum depth distribution which provided by the test system is illustrated in Fig. 6.

| Parameters                  | Values          |
|-----------------------------|-----------------|
| Maximum Load               | 3.00 mN         |
| Limit stop load            | 0.15 mN         |
| Initial load               | 0.05 mN         |
| Loading rate               | 0.10 mN/s       |
| Unloading rate             | 0.10 mN/s       |
| Indentations               | 18              |
| Dwell period at maximum load| 5 s             |

Table 1. Parameters setting in indentation procedure.

| Parameters                  | Values          |
|-----------------------------|-----------------|
| Maximum Load (nN)           | 3.054 ± 0.007   |
| Maximum Depth (nm)          | 77.68 ± 2.06    |
| Hardness (GPa)              | 12.577 ± 0.759  |
| Reduced modulus (GPa)       | 169.818 ± 4.911 |

Table 2. Test results.
The experimental loading-unloading curves show that there is one group of curve which is in bias with the bulk of the data. This inconsistent will be further discussed in the following uncertainty analysis part.

**Discussion**

**Analysis of unloading curves.** Errors estimation is a basic issue in the experiment uncertainty evaluation. In this study, the interest quantities of SWCNT film hardness $H$ and reduced elastic modulus $E_r$ are derived from the direct measurand of indentation loads and displacements. Parameters in the power law model (6) are obtained by making a power function regression analysis for the test data between 100% and 30% of unloading process, as shown in Fig. 7. The estimated parameters of model (6) for each set of indentation are given in Table 3.

**Parameters distribution analysis.** Data distribution of parameter $\alpha$, $h_f$, and $m$ in Table 3 are characterized by distribution graph in Fig. 8. After analyzing the probability distribution of $\alpha$, $h_f$, and $m$ we preliminarily hypothesize that $h_f$ may obeys the lognormal distribution and $m$ may obey the normal distribution, that is:

\[
\ln \alpha \sim N(\mu_\alpha, \sigma_\alpha^2)
\]

\[
\ln h_f \sim N(\mu_{h_f}, \sigma_{h_f}^2)
\]

\[
m \sim N(\mu_m, \sigma_m^2)
\]

By fitting the probability distribution of the values of $\alpha$, $h_f$, and $m$ in Table 3 to the hypothesized distribution, $\mu_\alpha$ and $\sigma_\alpha$ are equal to $-6.42$ and $0.19$, respectively; and $\mu_{h_f}$ and $\sigma_{h_f}$ are equal to $2.87$ and $0.22$, respectively. Table 4 gives the 0.95 level of confidence interval for $h_f$ and $m$.

For testing whether parameter $\alpha$, $h_f$, and $m$ in Table 3 follow the expected probability distribution, a goodness of fit test by using the Kolmogorov-Smirnov and Monte Carlo simulation method are carried out. The comparison
of empirical and theoretical fitted distributions for parameters distribution is illustrated in Fig. 9, it shows that the probability distributions of $\alpha$, $h_f$, and $m$ fit the hypothesized distribution very well.

**Uncertainty analysis for unloading process curve.** Based on the statistic estimation of parameter $\alpha$, $h_f$, and $m$ distribution we characterize the load-displacement curve for the 70% upper part of unloading process using Monte Carlo simulation method. Figure 10 is the comparison of the experimental and the simulation with a sample size of 5000 load-displacement curves for the upper part of unloading process. Comparison in Fig. 10 illustrates that experimental curves are rigorously inside the 95% confidence interval of the numerical simulation results, which demonstrates that the power law fitting model according well with the test results.

**Uncertainty estimation for Elastic modulus and hardness of SWCNT thin film.** In equations (1) and (4), the contact area A is calculated from the contact depth $h_c$, which is related to the total displacement $h_{\text{max}}$ of indenter:

$$h_c = h_{\text{max}} - \varepsilon \left( \frac{P_{\text{max}}}{S} \right)$$

(11)
here the contact stiffness $S$ is equals to the tangent at the maximum load.

$$S = \frac{dP_{\text{max}}}{dh_{\text{max}}} = m\alpha(h_{\text{max}} - h_f)^{m-1}$$  \hspace{1cm} (12)$$

The value of $\varepsilon$ depends on the indenter geometry. For a Berkovich indenter $\varepsilon$ is 0.75\textsuperscript{17}.

Area calibration and uncertainty evaluation. The area calibration relates the actual, non-ideal diamond contact area to the depth of penetration. The target of the area calibration is to find the function which can be

| Parameter | $\alpha$ | $h_f$ | $m$ |
|-----------|---------|-------|-----|
| Mean      | 0.00165 | 18.15689 | 1.846 |
| Confidence interval | [0.00112, 0.00214] | [10.71969, 25.28685] | [1.762, 1.930] |

Table 4. 95% confidence interval by parametric bootstrap method.
Figure 9. Parameter distribution. (a,c,e) The empirical CDF distribution and theoretical CDF distribution of the hypothesized function; (b,d,f) Comparison of empirical and theoretical fitted distribution.

Figure 10. Comparison of the simulation and experimental load-displacement curve for unloading process.
used across a wide indentation range to obtain accurate hardness and modulus values. In this study, the diamond area \( A \) is calculated using a polynomial function of order 2:

\[
A = c_0 h_c^2 + c_1 h_c + c_0
\]

(13)

For an ideal Berkovitch indenter, \( c_2 = 24.5 \), \( c_1 = c_0 = 0 \). A real Berkovitch indenter, although each diamond is slightly different, the typical values are \( c_2 = 20 \sim 24 \), \( c_1 = 1500 \sim 3000 \). Here \( c_2 = 21.93 \), \( c_1 = 2330.6 \), and \( c_0 = 52726.9 \).

According to the uncertainty propagation law, the standard area uncertainty \( \mu(A) \) can be expressed as:

\[
\left[ \mu(A) \right]^2 = (2c_0 h_c + c_1) \times [\mu(h_c)]^2 + \mu_\Delta^2
\]

(14)

where \( \mu_\Delta \) is the residuals of fitting curve, and \( [\mu(h_c)] \) is the uncertainty of contact depth which can be derived from equation (11):

\[
[\mu(h_c)]^2 = [\mu(h_{max})]^2 + \left[ \frac{e}{S} \mu(F_{max}) \right]^2 + \left[ \frac{e}{S^2} F_{max} \mu(S) \right]^2
\]

(15)

where \( \mu(h_{max}) \) is the uncertainty of maximum contact depth \( \mu(F_{max}) \) is the uncertainty of maximum applied load and \( \mu(S) \) is the uncertainty of contact stiffness

\[
[\mu(S)]^2 = \text{max}(m-1)(h_{max} - h_j)^{m-2} [\mu(h_{max})^2 + \mu(h_j)^2]
\]

\[
+ m(h_{max} - h_j)^{m-1} [\mu(\alpha)]^2 + \alpha \ln(m-1)(h_{max} - h_j)(\mu(m))^2
\]

(16)

In this study, the standard maximum load uncertainty \( \mu(F_{max}) \) and the standard maximum contact depth uncertainty \( \mu(h_{max}) \) are calculated by the standard deviation of 18 nodes indentation test. As the parameter distribution analysis in section 4.1.1 stated that \( \alpha \) and \( h_j \) follow a lognormal distribution the uncertainty are calculated as the root of the variance \( \mu(\alpha) = 0.00032 \), \( h_j = 4.024 \text{ nm} \), and \( \mu(m) = 0.042 \), the uncertainty of \( F_{max} \) and \( h_{max} \) are \( \mu(F_{max}) = 0.0069 \text{ mN} \), \( \mu(h_{max}) = 0.4851 \text{ nm} \). So

\[
\mu(S) = 4.75 \text{ nm}
\]

Uncertainty of hardness evaluation. The uncertainty of indentation hardness \( \mu(H) \) can be obtained from equation (1):

\[
[\mu(H)]^2 = \left[ \frac{1}{A} \mu(F_{max}) \right]^2 + \left[ \frac{F_{max}}{A^2} \mu(A) \right]^2
\]

(18)

Then the relative standard uncertainty of indentation hardness is:

\[
\left[ \frac{\mu(H)}{H} \right]^2 = \left[ \frac{\mu(F_{max})}{F_{max}} \right]^2 + \left[ \frac{\mu(A)}{A} \right]^2
\]

(19)

Uncertainty of reduced modulus evaluation. The uncertainty of reduced modulus \( \mu(E_r) \) can be obtained from equation (4)

\[
[\mu(E_r)]^2 = \left[ \frac{\sqrt{\pi}}{2 \sqrt{A}} \mu(S) \right]^2 + \left[ \frac{\sqrt{\pi}}{4 A^{3/2}} \mu(A) \right]^2
\]

(20)

The relative standard uncertainty of reduced modulus can be calculated by

\[
\left[ \frac{\mu(E_r)}{E_r} \right]^2 = \left[ \frac{\mu(S)}{S} \right]^2 + \left[ \frac{1}{2} \frac{\mu(A)}{A} \right]^2
\]

(21)

The uncertainty analysis results reveal that the relative expanded uncertainty of hardness and reduced modulus corresponding to a level of confidence of 95% are separately 12.07% and 10.64%. The dispersion of hardness and reduced modulus are much larger than the tested values that automatically obtained by the indentation system in Table 2.

Uncertainty of Young's modulus evaluation. The Young's modulus \( E \) is obtained from equation (7), which depends not only on the reduced modulus \( E_r \) but also on the modulus of indentor and the Poisson's ratio of the sample. According to the literatures, Young's modulus of Polycrystalline diamond changes from 1106 GPa to 1164 GPa, which depends on the orientation of structures. For the randomly orientated aggregates of diamond crystallites, it has the mean modulus and Poisson’s ratio of \( E_r = 1143 \text{ GPa} \), \( \varphi = 0.07 \). While, the Poisson's ratio of SWCNT sheets depend on the inter-tube torsional angle and the tubes orientation to sheet plan. The uncertainty of the Young's modulus of SWCNNTs thin film \( \mu(E) \) can be obtained from equation (7).
Table 5. The relative expanded standard uncertainty of parameters with a level of confidence of 95%.

| Parameter | Relative expanded standard uncertainty |
|-----------|---------------------------------------|
| μ(A)      | 7.94%                                 |
| μ(H)      | 12.07%                                |
| μ(E)      | 10.64%                                |
| μ(E)      | 13.54%                                |

\[
(\mu(E))^2 = 2\nu^2 \left( \frac{1}{E_f} - \frac{1 - \nu^2}{E_i} \right) \cdot \mu(v)^2 + (1 - \nu^2)^2 \left( \frac{1}{E_f} - \frac{1 - \nu^2}{E_i} \right)^2 \cdot \mu(E)^2 + (1 - \nu^2)^2 (1 - \nu^2)^2 \left( \frac{1}{E_f} - \frac{1 - \nu^2}{E_i} \right)^2 \cdot \mu(E)^2
\]  

The relative standard uncertainty of the Young's modulus can be calculated by

\[
\left( \frac{\mu(E)}{E} \right)^2 = \frac{2\nu^2}{(1 - \nu^2)^2} \cdot \mu(v)^2 + \left( 1 - \frac{(1 - \nu^2)}{E_i} \right)^2 \cdot \mu(E)^2
\]  

Here, for a standard diamond indenter probe, \( E_f = 1143 \) GPa, and \( v_i = 0.07 \). Some researchers also take \( E_f = 1100 \) GPa in literatures14. We suppose that the uncertainty of indenter's Young's modulus is about 0.038 percent at most, and the uncertainty is assumed to be uniformly distributed, and the standard uncertainty of Poisson's ratio \( \mu(v) = 0.069 \).

The relative expanded standard uncertainty of the diamond area, hardness, reduced modulus, and Young's modulus corresponding to a level of confidence of 95% are summarized in Table 5.

Conclusions
In this study, the elastic properties of SWCNT thin film (~250 nm) are studied by nanoindentation test. SWCNT thin films are prepared by the easy operated method of spin-coating technique and heat treatment. Hardness and young's modulus of the SWCNT thin film are well tested. The uncertainty of hardness and Young's modulus of SWCNT film is evaluated. The experimental results and uncertainty analysis reveal that the relative expanded uncertainty of hardness and Young's modulus of SWCNT thin film corresponding to a level of confidence 95% are separately 12.07% and 13.54%. The tested hardness and elastic modulus of SWCNT thin films are 12.577 ± 1.517 GPa and 192.83 ± 26.11 GPa, respectively. The uncertainty analysis indicates that nanoindentation test could be an effective and reliable technology in determining the mechanical properties of SWCNT thin film. This also suggests that nanoindentation technique could be a recommended method in determining properties of other nano scaled films.

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**Author Contributions**
C.R.S. and X.L.T. designed the research; X.L.T. and M.E. performed the experiments; C.R.S., A.E. and M.E. analyzed the data; A.E. and K.E. drew the figures; X.L.T. and C.R.S. wrote the paper; All authors commented on the manuscript.

**Additional Information**

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