1. Introduction

The constant increase in demands on the load capacity of railway structures leads to greater stiffness of construction layers and subgrade. Concrete sleepers are also almost exclusively used, because they have much higher bending stiffness and less flexibility than wooden sleepers. All these factors lead to greater loading on track bed, which changes its shape under increasing load and thereby affects the track geometry parameters. In the ballast track, for the reasons described above, gravel bench behind the heads of sleepers tends to collapse. Open spaces between the sleeper and gravel are created, due to the high bending stiffness of concrete sleepers. When a train passes the sleepers rest on the collapsed gravel bench, which creates uneven sleeper support and enhances the dynamic effects, which accelerates the degradation of track bed [1].

To avoid such undesirable phenomena as much as possible, considerable financial resources must be expended to new designs research, as well as to diagnostic quality of track geometry and their potential maintenance [2]. Still, there are some relatively simple measurement procedures, which can well predict the characteristics of the rail fastening and thus also its suitability. The aim of this paper is to point out the use of selected methods of experimental modal analysis to determine the characteristics of rail fastening.

2. Methods of measurement

The basic objective of methodology was comparison of rail fastening test samples in a laboratory with respect to the vibration response of the results obtained in situ. The method of excitation with impulse hammer was selected. The measured data were analysed using the Frequency Response Function (FRF) [3]. The dynamic responses were measured on the foot rail, on the head of the sleeper and in gravel ballast (except in-situ measurement).

A part of a sleeper with installed fastening system was used as a test sample in the laboratory. The sleeper was placed in gravel bed in shape of a truncated pyramid, which was built in a test box with dimensions of 2.0 x 2.0 m. The test box was insulated from the base plate by an interlayer of cork.

Furthermore, additional measurements were carried out in situ. For these purposes was selected a test section on line no 260 in the km 166.140 in the area of Bilovice nad Svitavou [4]. For obvious reasons, the exciting with impulse hammer was used in situ too.

3. Test samples

In the laboratory, the following types of baseplatesless flexible rail fastening for system UIC 60 and gauge extension + RK 0 mm were tested [5 and 6]:

1. The part of the sleeper B91P with Fastclip fastening and side insulator 7049
   • The fastening Pandrol (flexible clips, FC1501 with insulators 8494, pad under bottom rail 6530)
2. The part of the sleeper B91S/1 with polyamide opened plug
   • The fastening system Vossloh W14 (flexible clamps Skl14, angled guides Wfp 14K-12, sleeper screw R1 with pad Uls 7, pad under bottom of the rail WU 7)
The fastening system Vossloh W14NT (flexible clamps Skl14, angled guides Wfp 14K NT, sleeper screw R1 with pad Uls 7, pad under bottom of the rail Zw 900 NT)

The fastening system Vossloh W21NT (flexible clamps Skl21, angled guides Wfp 21K NT-12, sleeper screw R1 with pad Uls 7, pad under bottom of the rail Zw 1000/150 HS-35)

The fastening system Vossloh E14 (flexible clamps Skl 21, angled guides Wfp 16G/Wfp 16F, sleeper screw R3 with pad Uls 7, pad under bottom of the rail Zw 693/150, steel spread plate Grp 22/150, highly flexible pad Zwp E14 NT/150).

Verifying measurements in situ were performed on fastening Vossloh W14 in track No. 1, or on fastening Pandrol FC I in track No. 2 of the given section of the track. The rail fastening Pandrol FC I and especially Vossloh W14 are the most commonly used without-clip-plate flexible fastenings in the Czech Republic. These can be found in all the upgraded sections of transit railway corridors and tracks of national importance.

Fastening W14NT is equipped with angled guide inserts Wfp 14K NT provided with a special guide rail on the underside. This guide rail in the mounting position enters the area under the track base, avoiding excessive tipping or decline of the track. For this reason, the fastening W14NT is preferably used in track with directional arcs of small radii. Fastening E14 belongs among the fastenings with increased vertical flexibility.

Fastenings E14 is suitable where there is a need to increase the damping of dynamic effects or reduce the emitted noise. It was originally developed for slab track where highly elastic pad Zwp E14 NT/150 replaced the dampening effects of the entire track bed. Currently the trend for fastenings E14 can be observed also in places where it is not possible to establish a sufficient track bed thickness. It is a fastening with a highly elastic underlay under the track base Zw 1000/150 HS-35. This increased flexibility is also consistent with vertical higher fatigue limit of clamps Skl21. Field of application of fastening W21NT is similar to fastening W14NT or E14.

4. The test arrangement

Laboratory samples were fitted with rail grid vibration acceleration sensors as shown in Fig. 1. From the perspective of the cross section all sensors were placed in the longitudinal axis of the sleepers. Location of sensors Ar and As was due to the rail web chosen conceptually in accordance with previous measurements [7 and 8]. A special measuring stone was developed at the Institute of Railway Structures and Constructions, due to the location of the sensor Agb to the gravel beneath the mattress platform of sleeper. The Agb sensor was not used in measuring in-situ. The in-situ test arrangement is shown in Fig. 2.

Suitable Bruel&Kjaer accelerometers (type BK 4507B004) were used as sensors. Impact was driven with the impact hammer Bruel&Kjaer, type 8210, with excitation tip hard tip black. Data from measurement were analysed using PULSE 3560D modular analyser from Bruel & Kjaer.

5. Evaluation of the data

The results are partially shown in Tables 1 - 2 and Fig. 3. Assessed value of impulse excitation was the accelerance. Frequency range 1 - 1000 Hz was set after the initial testing. In the case of impulse evaluation three repeated laboratory measurements of accelerance were performed for each type of rail fastening, each derived from ten hammer hits. Impulse hammer was used also in the case of the verification in situ. Frequency and survey methodology of accelerance measurement was similar to that in the laboratory. However, in order to guarantee safe
operation of the track, the influence of the tightening of the propeller was not measured at Vossloh fastening.

The results of individual measurements were averaged and displayed in graphs of frequency response functions H3. Relative damping (damping ratio) of tested structures was determined by half-power bandwidth method. Evaluation was done in software ME'Scope. It is worth noting that the Tables 1 and 2 contain full results for rail fastenings Pandrol FC I and Vossloh W14 only.

The evaluation focused on the low-frequency range of 1 ÷ 80 Hz, medium-frequency range 80 ÷ 400 Hz and high-frequency range of 400 ÷ 1000 Hz. This division is based on previous work and is based on the principle that in the low frequency range mainly the effects of the operation of bogies and wheelsets of moving railway vehicles can be observed, middle frequency range is a manifestation of imperfections on the wheel rail contact area, as well as a high frequency range up to 1000 Hz. Here, however, the influence of acoustic phenomena caused by moving vehicles is also manifested.

In the low-frequency range all fastening systems show a significant response between 60 and 80 Hz. The most significant relative damping on the rail 5.3% is achieved with Vossloh fastening W14NT, the smallest 0.8% with fastening Vossloh E14. High damping ratio of fastening W14NT is most likely caused by the guide rail on the bottom surface of the angular guide insert that prevents larger rail movements. On the contrary, the fastening E14 is characterised by an increased vertical flexibility, which may result in increased vibration of the rail. On the sleeper there was the largest structural damping 9.3% recorded at fastening Vossloh W21NT, the smallest at Pandrol FC I and at Vossloh W14NT (both 3.1%). The difference between the damping on the rail and on the sleeper can indicate vertical fastening flexibility. Vossloh fastening E14 W and Vossloh W21NT can therefore be defined as the fastening with largest vertical flexibility. The resulting damping 4.3 ± 2.2% in the track bed suggests that the densified layer of gravel created stable surface for all tested sets.

There are no significant frequencies for fixing Pandrol FC I on the rail at the medium frequency range, except for frequency 277 Hz in situ, where the tested structure shows a damping of 3.1%. This frequency is equivalent to a frequency of 430 Hz, which was recorded in laboratory tests. On the sleeper there are significant frequency ranges of fastening Pandrol frequencies of 145 ÷ 165 Hz, where it reaches an average damping of 5.3%. Greater damping at high frequencies in the track bed was not reached. Neither at Vossloh rail fastening W14 significant frequency was found. This fastening achieves an average damping of 3.7% on sleeper In this respect, the range of 110 ÷ 215 Hz is particularly important. Damping of 6.4% at frequencies of 115 ÷ 155 Hz in gravel was calculated. Fastening W14NT shows damping 4.0% on the rail, 3.4% on the sleeper and 4.2% in the track bed at selected frequencies in the range 110 ÷ 340 Hz. For fastening Vossloh W21NT the essential resonance frequency is 290 Hz. Fastening here shows damping of 7.3% on the rail, 6.3% on the sleeper and 7.4% in the gravel. Another frequency spectrum of 130 ÷ 145 Hz is not so important; the construction here achieves damping 4.5%.

The last tested construction Vossloh E14 shows a high resonant range 120 ÷ 130 Hz with damping 3.6% on the rail, 3.1% on the sleeper and 3.9% in the track bed. Even more significant damping of about 5.2% was obtained at a frequency of 220 ÷ 265 Hz. Overall, the comparison of the behaviour of structures reveals that with increasing vertical fastening flexibility the size of the resonance range of medium frequencies of 80 to 400 Hz increases as well. The least favourable in this respect seems to be W21NT Vossloh fastening, fixing Pandrol FC I, or Vossloh fastening E14.

For fastening Pandrol FC I the frequency 430 Hz is important in the higher frequency range of 400 ÷ 1000 Hz, where the average damping is 2.6% and in track bed also frequencies 630 ÷ 730 Hz with the calculated damping of 1.9%. For fastening Vossloh W14 damping was found at the large number of high-frequency range. Only the values of range 450 ÷ 500 Hz and 600 ÷ 700 Hz are, however, higher than 1.0%.

For fastening Vossloh W14NT damping was found in the frequency range 510 Hz to 600 Hz in the average of 1.5%.

The relative damping in dependence on the frequency. Pandrol FC I fastening

| Sensor | Laboratory, Impact excitation | In situ, Impact excitation |
|--------|-------------------------------|----------------------------|
|        | f [Hz] Damping [%] | f [Hz] Damping [%] |
| **Rail Ar** |                   |                  |
| 69    | 3.0               | 83               | 3.3 |
| 167   | 1.3               | 277              | 3.1 |
| 430   | 3.1               | 359              | 0.4 |
| 573   | 0.1               | 518              | 0.6 |
| 650   | 0.1               | 774              | 0.5 |
| 701   | 0.1               | 931              | 0.1 |
| **Sleeper As** |                   |                  |
| 73    | 4.0               | 64               | 2.1 |
| 114   | 1.7               | 147              | 7.7 |
| 165   | 2.6               | 278              | 4.6 |
| 422   | 5.6               | 591              | 0.1 |
| 651   | 0.1               | 773              | 0.1 |
| 874   | 0.1               | 798              | 0.1 |
| **Gravel ballast AbB** |                   |                  |
| 70    | 2.8               | -                | -   |
| 89    | 2.8               | -                | -   |
| 198   | 2.4               | -                | -   |
| 222   | 1.3               | -                | -   |
| 437   | 5.3               | -                | -   |
| 733   | 4.5               | -                | -   |
| 850   | 0.2               | -                | -   |
Internal damping of 3.3% of the corresponding frequencies 410 ÷ 445 Hz was also found in track bed. The average damping value of 1.9% was calculated for Vossloh fastening system W21NT. This damping was achieved at frequencies of 415 ÷ 445 Hz. The second major frequency is 562 Hz, where the damping of 3.3% was found. Fastening E14 showed in the selected frequency range 400 ÷ 1000 Hz no significant damping values exceeding 0.5%. In the range of higher frequencies all tested fastenings show the diminished ability of vibration damping than in the range below 400 Hz. The least favourable of all tested structures seems to be Vossloh fastening W14NT that in 510 Hz to 600 Hz shows the highest amplitude of the vibration acceleration on the sleeper, hence in the track bed.

From the waveform of frequency response functions it is possible to determine the characteristics indicative for the test of rail fastening in terms of their mounting rigidity and in terms of relative acceleration of the rail towards the sleeper in a vertical direction by quantifying surface between curves \( A_r \) and \( A_s \). The presence of the guides on the underside of the guide angle insert fastenings W14NT and W21NT using low frequency range up to 80 Hz which causes a very small area between the given curves in this frequency range - relative vertical vibration acceleration transmission from the track to the sleeper is minimal.

In the overall frequency scale, the largest differences between the curves \( A_r \) and \( A_s \) are at fastenings E14, the smallest at fastenings W14. Measurement tentatively confirmed the static cutting stiffness of tested sets of rail fastenings listed in company regulations.

Fastening Pandrol FC I shows interesting properties in the resonant frequency range of around 430 Hz. This frequency is a manifestation of corrugation with a period of waves about 7 ÷ 9 cm, depending on the driving speed, which is considered in the range typical for corridor route, i.e. 120 to 160 km·h\(^{-1}\). Using the fastenings Pandrol FC I on routes where there is emergence of corrugation with that wavelength, can accelerate the development of rail defects. Similar characteristics are also shown by fastenings Vossloh W21NT at high frequencies around 290 Hz or by Vossloh fastenings E14 at frequencies in the range of 220 ÷ 265 Hz.

At the tested fastenings with maximum static secant stiffness Vossloh W14 and Vossloh W14NT there is the most noticeable shift of resonant range towards higher frequencies. The presence of waves of shorter wavelengths up to 5 cm can be seen on the corridor lines in the high frequency range. Therefore it follows that in areas where we can expect the development of periodic defects of the rail surface of small and medium-sized lengths it is, due to general properties, suitable to use vertical flexible fastening systems, such as Vossloh E14 or Vossloh W21NT. On the contrary, in places where we can expect rail defects like gliding or long waves, it is preferable to use fastenings with higher static secant stiffness of the rail pad. These include fastening system Vossloh W14, whether made with a guide rail on the underside of the angular guide insert (type NT) or without.

### Table 2

| Sensor   | Laboratory, Impact excitation | In situ, Impact excitation |
|----------|-------------------------------|---------------------------|
|          | f [Hz] Damping [%] f [Hz] Damping [%] |
| Rail At  |                               |                           |
| 72       | 2.3                           | -                         |
| 128      | 2.3                           | 119 1.0                   |
| 497      | 0.4                           | 595 0.6                   |
| 646      | 0.2                           | 752 0.1                   |
| 772      | 0.3                           | 781 1.0                   |
| 830      | 0.2                           | 802 1.8                   |
| 905      | 0.1                           | 906 0.1                   |
| Sleeper At |                               |                           |
| 74       | 6.1                           | -                         |
| 96       | 3.2                           | 149 6.2                   |
| 112      | 3.7                           | 305 0.3                   |
| 215      | 3.1                           | 473 0.1                   |
| 499      | 6.9                           | 583 0.1                   |
| 633      | 0.5                           | 792 0.1                   |
| 772      | 0.3                           | 803 0.1                   |
| 831      | 0.2                           | -                         |
| 834      | 0.1                           | -                         |
| Gravel ballast Agb |                   |                           |
| 40       | 1.6                           | -                         |
| 72       | 4.5                           | -                         |
| 85       | 2.2                           | -                         |
| 146      | 4.2                           | -                         |
| 222      | 0.3                           | -                         |
| 500      | 0.4                           | -                         |
| 699      | 0.2                           | -                         |
| 751      | 0.1                           | -                         |
| 821      | 0.1                           | -                         |

6. Conclusion

Carried out laboratory and operational measurements showed stable performance of all tested types of fastenings for the range of testing. Dependence on the size of the static cutting stiffness and resonant field of fastening systems was revealed. The firmer the fastening the more is the range of the most important frequencies shifted towards higher frequencies.

From the above it can be concluded that, for example, in the Czech Republic operationally validated fastening type Vossloh...
Fig. 3 Frequency characteristics of the testing samples rail fastening, standard tightening torque

Vossloh E14 - labo, impact excitation
Rail Ar  Sleeper As  G. Ballast Agb

Vossloh W14 - labo, impact excitation
Rail Ar  Sleeper As  G. ballast Agb

Vossloh W14NT - labo, impact excitation
Rail Ar  Sleeper As  G. ballast Agb

Vossloh W21 NT - labo, impact excitation
Rail Ar  Sleeper As  G. ballast Agb

Vossloh E14 - labo, impact excitation
Rail Ar  Sleeper As
and stresses in continuous welded rail, which was not taken into account in measurements under laboratory conditions. Slightly different characteristics of both analysed fastenings in higher frequency ranges are then probably also related to the generally complex ties rail - sleeper - rail bed in situ, which cannot be fully simulated under laboratory conditions.

Based upon the analyses made it is possible to say that the used methods offer good results and conclusions. The measured and calculated values prove to be sufficiently accurate and have excellent testing ability.

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