DARA: DYNAMICS-AWARE REWARD AUGMENTATION IN OFFLINE REINFORCEMENT LEARNING

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ABSTRACT

Offline reinforcement learning algorithms promise to be applicable in settings where a fixed dataset is available and no new experience can be acquired. However, such formulation is inevitably offline-data-hungry and, in practice, collecting a large offline dataset for one specific task over one specific environment is also costly and laborious. In this paper, we thus 1) formulate the offline dynamics adaptation by using (source) offline data collected from another dynamics to relax the requirement for the extensive (target) offline data, 2) characterize the dynamics shift problem in which prior offline methods do not scale well, and 3) derive a simple dynamics-aware reward augmentation (DARA) framework from both model-free and model-based offline settings. Specifically, DARA emphasizes learning from those source transition pairs that are adaptive for the target environment and mitigates the offline dynamics shift by characterizing state-action-next-state pairs instead of the typical state-action distribution sketched by prior offline RL methods. The experimental evaluation demonstrates that DARA, by augmenting rewards in the source offline dataset, can acquire an adaptive policy for the target environment and yet significantly reduce the requirement of target offline data. With only modest amounts of target offline data, our performance consistently outperforms the prior offline RL methods in both simulated and real-world tasks.

1 INTRODUCTION

Offline reinforcement learning (RL) (Levine et al., 2020; Lange et al., 2012), the task of learning from the previously collected dataset, holds the promise of acquiring policies without any costly active interaction required in the standard online RL paradigm. However, we note that although the active trial-and-error (online exploration) is eliminated, the performance of offline RL method heavily relies on the amount of offline data that is used for training. As shown in Figure 1, the performance deteriorates dramatically as the amount of offline data decreases. A natural question therefore arises: can we reduce the amount of the (target) offline data without significantly affecting the final performance for the target task?

Bringing the idea from the transfer learning (Pan & Yang, 2010), we assume that we have access to another (source) offline dataset, hoping that we can leverage this dataset to compensate for the performance degradation caused by the reduced (target) offline dataset. In the offline setting, previous work (Siegel et al., 2020; Chebotar et al., 2021) has characterized the reward (goal) difference between the source and target, relying on the "conflicting" or multi-goal offline dataset (Fu et al., 2020), while we focus on the relatively unexplored transition dynamics difference between the source dataset and the target environment. Meanwhile, we believe that this dynamics shift is not arbitrary in reality: in healthcare treatment, offline data for a particular patient is often limited, whereas we can obtain diagnostic data from other patients with the same case (same reward/goal)
The image contains a text document discussing the challenges and solutions in offline reinforcement learning (RL). The text highlights the importance of addressing individual differences between patients and the difficulties in strictly tracking state-action supported by source offline data. It introduces the concept of dynamics shift and the need for a reward modification approach that accounts for both state-action and dynamics shifts. The document outlines an approach called DARA (Dynamics-Aware Reward Augmentation) that can be implemented in a few lines of code and is designed to improve performance in both simulated and real-world tasks. The text also touches on related work, categorizing offline RL methods into model-free and model-based approaches and discussing their limitations. The document concludes with the presentation of a dynamics shift dataset that includes tasks with dynamics (mass, joint) shift compared to D4RL and a 12-DoF quadruped robot in both simulator and real-world settings.
3 Preliminaries

We study RL in the framework of Markov decision processes (MDPs) specified by the tuple \( M := (\mathcal{S}, \mathcal{A}, r, T, \rho_0, \gamma) \), where \( \mathcal{S} \) and \( \mathcal{A} \) denote the state and action spaces, \( r(s, a) \in [-R_{max}, R_{max}] \) is the reward function, \( T(s'|s, a) \) is the transition dynamics, \( \rho_0(s) \) is the initial state distribution, and \( \gamma \) is the discount factor. The goal in RL is to optimize a policy \( \pi(a|s) \) that maximizes the expected discounted return \( \eta_M(\pi) := \mathbb{E}_{\tau \sim P^\pi_T} \left[ \sum_{t=0}^{\infty} \gamma^t r(s_t, a_t) \right] \), where \( \tau := (s_0, a_0, s_1, a_1, \ldots) \). We also define Q-values \( Q(s, a) := \mathbb{E}_{\tau \sim P^\pi_T} \left[ \sum_{t=0}^{\infty} \gamma^t r(s_t, a_t) \mid s_0 = s, a_0 = a \right] \).

In the offline RL problem, we have a static dataset \( D := \{(s, a, r, s')\} \), which consists of transition tuples from trajectories collected by running one or more behavioral policies, denoted by \( \pi_b \), on MDP \( M \). With a slight abuse of notation, we write \( D := \{(s, a, r, s') \sim d_D(s)\pi_b(a|s)r(s, a)T(s'|s, a)\} \), where \( d_D(s) \) denotes state-marginal distribution in \( D \). In the offline setting, the goal is typically to learn the best possible policy using the fixed offline dataset.

Model-free RL algorithms based on dynamic programming typically perform policy iteration to find the optimal policy. Such methods iteratively conduct 1) policy improvement with \( \pi \), and 2) evaluation by iterating \( Q \)-functions \( E^Q \). Given off-policy \( D \), we resort to 1) improvement with \( \pi \) and 2) evaluation by iterating \( Q \)-functions \( E^Q \).

\[
\pi^{k+1} = \hat{\pi}^D Q^k, \quad \text{Policy evaluation:} \quad Q^{k+1} = B^D_{\pi} Q^k. \tag{1}
\]

Model-free offline RL: Based on the above iteration suffers from the state-action distribution shift, i.e., policy evaluation \( B^D_{\pi} Q^{k-1} \) may encounter unfamiliar states and transitions that are not covered by the fixed offline dataset \( D \), causing erroneous estimation of \( Q^k \). Policy improvement \( \hat{\pi}^D Q^k \) further exaggerates such error, biasing policy \( \pi^{k+1} \) towards out-of-distribution (OOD) actions with erroneously high Q-values. To address this distribution shift, prior works 1) explicitly constrain policy \( \pi^D \) to be close to the behavior policy \( \{\tilde{T}_{\pi}, \tilde{r}, \tilde{\mathcal{D}}\} \), using MMD or KL divergence, or 2) train pessimistic value functions \( \{\tilde{T}_{\pi}, \tilde{r}, \tilde{\mathcal{D}}\} \), penalizing Q-values at states in the offline dataset \( D \) for actions generated by the current policy \( \pi^D \).

\[
\pi^{k+1} = \hat{\pi}^D Q^k, \quad \text{Policy evaluation:} \quad Q^{k+1} = B^D_{\pi} Q^k. \tag{1}
\]

Model-based RL algorithms iteratively 1) model the transition dynamics \( T(s'|s, a) \), using the data collected in \( M \): \( \max_{\hat{T}} \mathbb{E}_{s, a, s' \sim \hat{T}} \log \hat{T}(s'|s, a) \), and 2) infer a policy \( \pi \) from the modeled \( \hat{M} = (\mathcal{S}, \mathcal{A}, r, T, \rho_0, \gamma) \), where we assume that \( r, T, \rho_0 \) are known, maximizing \( \eta_{\hat{M}}(\pi) \) with a planner or the Dyna-style algorithms \( \{\text{Sutton 1990}\} \). In this paper, we focus on the latter.

Model-based offline RL: Algorithms similarly suffer from OOD state-action \( \{\text{Kidambi et al. 2020}\} \) if we directly apply policy iteration over \( \hat{T} := \max_{\hat{T}} \mathbb{E}_{s, a, s' \sim \hat{T}} \log \hat{T}(s'|s, a) \). Like the conservative approximation described in Equation 3, recent conservative model-based offline RL methods provide the policy with a penalty for visiting states under the estimated \( T \) where \( \hat{T} \) is likely to be incorrect. Taking \( u(s, a) \) as the oracle uncertainty \( \{\text{Yu et al. 2020}\} \) provides a consistent estimate of the accuracy of model \( \hat{T} \) at \( (s, a) \), we can modify the reward function to obtain a conservative MDP: \( \hat{M}_c = (\hat{S}, \hat{A}, r - \alpha u, \hat{T}, \rho_0, \gamma) \), then learn a policy \( \pi \) by maximizing \( \eta_{\hat{M}_c}(\pi) \).

\[\text{For parametric Q-function, we often perform } Q^{k+1} \leftarrow \arg \min_{Q} \mathbb{E}_{s, a, s' \sim \hat{D}} [Q^k(s', a) - Q(s, a)]^2.\]
4 Problem Formulation

In standard offline RL problem, the static offline dataset $D$ consists of samples $\{(s, a, r, s') \sim d_D(s)\pi_b(a|s)r(s, a)T(s'|s, a)\}$. Although offline RL methods learn policy for the target MDP $M := (S, A, r, T, \rho_0, \gamma)$ without (costly) online data, as we shown in Figure 1, it requires a fair amount of (target) offline data $D$ collected on $M$. Suppose we have another (source) offline dataset $D'$, consisting of samples $\{(s, a, r, s') \sim d_D(s)\pi_b(a|s)r(s, a)T(s'|s, a)\}$ collected by the behavior policy $\pi_b'$ on MDP $M' := (S, A, r, T', \rho_0, \gamma)$, then we hope the transfer of knowledge between offline dataset $(D' \cup D)$ can reduce the data requirements on $D$ for learning policy for the target $M$.

4.1 Dynamics Shift in Offline RL

Although offline RL methods in Section 3 have incorporated the state-action distribution constrained backups (policy constraints or conservative estimation), they also fail to learn an adaptive policy for the target MDP $M$ with the mixed datasets $\{D' \cup D\}$, as we show in Figure 4 (Appendix). We attribute this failure to the dynamics shift (Definition 2) between $D'$ and $M$ in this adaptation setting.

Definition 1 (Empirical MDP) An empirical MDP estimated from $D$ is $\hat{M} := (S, A, r, \hat{T}, \rho_0, \gamma)$

Definition 2 (Dynamics shift) Let $\hat{M} := (S, A, r, \hat{T}, \rho_0, \gamma)$ be the empirical MDP estimated from $D$. To evaluate a policy $\pi$ for $M := (S, A, r, T, \rho_0, \gamma)$ with offline dataset $D$, we say that the dynamics shift (between $D$ and $M$) in offline RL happens if there exists at least one transition pair $(s, a, s') \in \{(s, a, s') : d_M(s)\pi(a|s)T(s'|s, a) > 0\}$ such that $T(s'|s, a) \neq T'(s'|s, a)$.

In practice, for a stochastic $M$ and any finite offline data $D$ collected in $M$, there always exists the dynamics shift. The main concern is that finite samples are always not sufficient to exactly model stochastic dynamics. Following Fujiimoto et al. (2019), we thus assume both MDPs $M$ and $M'$ are deterministic, which means the empirical $M$ and $M'$ are both also deterministic. More importantly, such assumption enables us to explicitly characterize the dynamics shift under finite offline samples.

Lemma 1 Under deterministic transition dynamics, there is no dynamics shift between $D$ and $M$.

For offline RL tasks, prior methods generally apply $B_D^\pi Q$ along with the state-action distribution correction (Equations 2 and 3), which overlooks the potential dynamics shift between the (source) offline dataset and the target MDP (e.g., $D' \to M$). As a result, these methods do not scale well to the setting in which dynamics shift happens, e.g., learning an adaptive policy for $M$ with (source) $D'$.

4.2 Dynamics Shift in Model-free and Model-based Offline Formulations

From the model-free (policy iteration) view, an exact policy evaluation on $M$ is characterized by iterating $Q(s, a) = B_D^\pi Q(s, a)$ for all $(s, a)$ such that $d_M(s)\pi(a|s) > 0$. Thus, to formalize the policy evaluation with offline $D$ or $D'$ (for an adaptive $\pi$ on target $M$), we require that Bellman operator $B_D^\pi Q(s, a)$ or $B_{D'}^\pi Q(s, a)$ approximates the oracle $B_M^\pi Q(s, a)$ for all $(s, a)$ in $S_\pi$ or $S'_\pi$, where $S_\pi$ and $S'_\pi$ denote the sets $\{(s, a) : d_D(s)\pi(a|s) > 0\}$ and $\{(s, a) : d_{D'}(s)\pi(a|s) > 0\}$ respectively.

1) To evaluate a policy $\pi$ for $M$ with $D$ (i.e., calling the Bellman operator $B_D^\pi$), notable model-free offline method BCQ (Fujiimoto et al. [2019]) translates the requirement of $B_D^\pi = B_M^\pi$ into the requirement of $T(s'|s, a) = T'(s'|s, a)$. Note that under deterministic environments, we have the property that for all $(s, a, s')$ in offline data $D$, $T(s'|s, a) = T'(s'|s, a)$ (Lemma 1). As a result, such property permits BCQ to evaluate a policy $\pi$ by calling $B_D^\pi$, replacing the oracle $B_M^\pi$, meanwhile constraining $S_\pi$ to be a subset of the support of $d_D(s)\pi_b(a|s)$. This means a policy $\pi$ which only traverses transitions contained in (target) offline data $D$, can be evaluated on $M$ without error.

2) To evaluate a policy $\pi$ for $M$ with $D'$ (i.e., calling the Bellman operator $B_{D'}^\pi$), we have lemma 2

Lemma 2 Dynamics shift produces that $B_{D'}^\pi Q(s, a) \neq B_M^\pi Q(s, a)$ for some $(s, a) \in S'_\pi$.

With the offline data $D'$, lemma 2 suggests that the above requirement $B_{D'}^\pi = B_M^\pi$ becomes infeasible, which limits the practical applicability of prior offline RL methods under the dynamics shift.
To be specific, characterizing an adaptive policy for target MDP $M'$ with $D'$ moves beyond the reach of the off-policy evaluation based on iterating $Q = B_{M'}^T Q$ (Equations 2 and 3). Such iteration may cause the evaluated $Q$ (or learned policy $\pi$) overfits to $T'$ and struggle to adapt to the target $T$. To overcome the dynamics shift, we would like to resort an additional compensation $\Delta_{F,T}$ such that

$$B_{M'}^T Q(s, a) + \Delta_{F,T}(s, a) = B_M^T Q(s, a)$$  \hspace{1cm} (4)

for all $(s, a)$ in $S_f$. Thus, we can apply $B_{M'}^T Q + \Delta_{F,T}$ to act as a substitute for the oracle $B_M^T Q$.

From the model-based view, the oracle $\eta_M(\pi)$ (calling the Bellman operator $B_M^T$ on the target $M$) and the viable $\eta_M(\pi)$ (calling $B_M^{T'}$ on the estimated $M'$ from source $D'$) have the following lemma.

**Lemma 3** Let $B_M^T V(s) = \mathbb{E}_{a \sim \pi(a|s)} [r(s, a) + \gamma \mathbb{E}_{s' \sim T(s'|s, a)} [V(s')]]$. For any $\pi$, we have:

$$\eta_M(\pi) = \eta_M(\pi) + \mathbb{E}_{a \sim \hat{d}_{M}^{T'}(s)} \left[ B_M^{T'} V_M(s) - B_M^{T'} V_M(s) \right].$$

Lemma 3 states that if we maximize $\eta_{M'}(\pi)$ subject to $|\mathbb{E}_{a \sim \hat{d}_{M}^{T'}(s)} [B_M^{T'} V_M(s) - B_M^{T'} V_M(s)]| \leq \epsilon$, $\eta_M(\pi)$ will be improved. If $F$ is a set of functions $f : S \to \mathbb{R}$ that contains $V_M$, then we have

$$\left| \mathbb{E}_{a \sim \hat{d}_{M}^{T'}(s)} \left[ B_M^{T'} V_M(s) - B_M^{T'} V_M(s) \right] \right| \leq \gamma \mathbb{E}_{a \sim \hat{d}_{M}^{T'}(s)} \left[ d_F(\hat{T}'(s'|s, a), T(s'|s, a)) \right]$$  \hspace{1cm} (5)

where $d_F(\hat{T}'(s'|s, a), T(s'|s, a)) = \sup_{f \in F} |\mathbb{E}_{s' \sim \hat{T}'(s'|s, a)} [f(s')] - \mathbb{E}_{s' \sim T(s'|s, a)} [f(s')]|$, which is the integral probability metric (IPM). Note that if we directly follow the admissible error assumption in MOPO [Yu et al. 2020] i.e., assuming $d_F(\hat{T}'(s'|s, a), T(s'|s, a)) \leq u(s, a)$ for all $(s, a)$, this would be too restrictive: given that $\hat{T}'$ is estimated from the source offline samples collected under $T'$, not the target $T$, thus such error would not decrease as the source data increases. Further, we find

$$d_F(\hat{T}'(s'|s, a), T(s'|s, a)) \leq d_F(\hat{T}'(s'|s, a), \hat{T}(s'|s, a)) + d_F(\hat{T}(s'|s, a), T(s'|s, a)).$$  \hspace{1cm} (6)

Thus, we can bound the $d_F(\hat{T}', T)$ term with the admissible error assumption over $d_F(\hat{T}', T)$, as in MOPO, and the auxiliary constraints $d_F(\hat{T}', T)$. See next section for the detailed implementation.

**In summary**, we show that both prior offline model-free and model-based formulations suffer from the dynamics shift, which also suggests us to learn a modification ($\Delta$ or $d_F$) to eliminate this shift.

5 DYNAMICS-AWARE REWARD AUGMENTATION

In this section, we propose the dynamics-aware reward augmentation (DARA), a simple data augmentation procedure based on prior (model-free and model-based) offline RL methods. We first provide an overview of our offline reward augmentation motivated by the compensation $\Delta_{F,T}$ in Equation 4 and the auxiliary constraints $d_F(\hat{T}', T)$ in Equation 6 and then describe its theoretical derivation in both model-free and model-based formulations. With the (reduced) target offline data $D$ and the source offline data $D'$, we summarize the overall DARA framework in Algorithm 1.

**Algorithm 1** Framework for Dynamics-Aware Reward Augmentation (DARA)

**Require**: Target offline data $D$ (reduced) and source offline data $D'$

1: Learn classifiers ($q_{\text{src}}$ and $q_{\text{trg}}$) that distinguish source data $D'$ from target data $D$. (See Appendix A.1.3)
2: Set dynamics-aware $\Delta_T(s_t, a_t, s_{t+1}) = \log q_{\text{trg}}(s_t, a_t, s_{t+1})^\text{source} \cdot q_{\text{src}}(s_t, a_t, s_{t+1})^{\text{target}} - \log q_{\text{trg}}(s_t, a_t) / q_{\text{src}}(s_t, a_t).
3: Modify rewards for all $(s_t, a_t, r_t, s_{t+1})$ in $D'$: $r_t \leftarrow r_t - \eta \Delta_T$.
4: Learn policy with $\{D \cup D'\}$ using prior model-free or model-based offline RL algorithms.

5.1 DYNAMICS-AWARE REWARD AUGMENTATION IN MODEL-FREE FORMULATION

Motivated by the well established connection of RL and probabilistic inference [Levine 2018], we first cast the model-free RL problem as that of inference in a particular probabilistic model. Specifically, we introduce the binary random variable $O$ that denotes whether the trajectory $\tau :=...
We define the bound of \( \log \pi(O = 1) \) or not \((O = 0)\). The likelihood of a trajectory can then be modeled as \( p(O = 1 | \tau) = \exp \left( \sum_t r_t / \eta \right) \), where \( r_t := r(s_t, a_t) \) and \( \eta > 0 \) is a temperature parameter.

**R(A)w(T)m(\( \Omega = 1 \))** We now introduce a variational distribution \( p^\pi_{\Omega} (\tau) = p(s_0) \prod_{t=1}^T T'(s_{t+1} | s_t, a_t) \pi(a_t | s_t) \) to approximate the posterior distribution \( p^\pi_{\Omega} (\Omega = 1) \), which leads to the evidence lower bound of \( \log p^\pi_{\Omega} (\Omega = 1) \):

\[
\log p^\pi_{\Omega} (\Omega = 1) = \log \mathbb{E}_{\tau \sim p^\pi_{\Omega} (\tau)} \left[ p(\Omega = 1 | \tau) \right] \geq \mathbb{E}_{\tau \sim p^\pi_{\Omega} (\tau)} \left[ \log p(\Omega = 1 | \tau) + \log \frac{p^\pi_{\Omega} (\tau)}{\pi_{\Omega}} \right] = \mathbb{E}_{\tau \sim p^\pi_{\Omega} (\tau)} \left[ \sum_t \left( r_t / \eta - \log \frac{T'(s_{t+1} | s_t, a_t)}{\pi(s_t | s_t, a_t)} \right) \right].
\]

(7)

Since we are interested in infinite horizon problems, we introduce the discount factor \( \gamma \) and take the limit of steps in each rollout, i.e., \( H \to \infty \). Thus, the RL problem on the MDP \( M \), cast as the inference problem \( \arg \max_\pi \log p^\pi_{\Omega} (\Omega = 1) \), can be stated as a maximum of the lower bound \( \mathbb{E}_{\tau \sim p^\pi_{\Omega} (\tau)} \left[ \sum_{t=0}^\infty \gamma^t \left( r_t - \eta \log \frac{T'(s_{t+1} | s_t, a_t)}{\pi(s_t | s_t, a_t)} \right) \right] \). This is equivalent to an RL problem on \( M' \) with the augmented reward \( r \leftarrow r(s, a) - \eta \log \frac{T'(s' | s, a)}{\pi'(s' | s, a)} \). Intuitively, the \( -\eta \log \frac{T'(s' | s, a)}{\pi'(s' | s, a)} \) term discourages transitions \((s, a, s') \) that have low transition probability in the target \( M \). In the model-free offline setting, we can add the explicit policy or Q-value constraints (Equations-2 and 3) to mitigate the OOD state-actions. Thus, such formulation allows the oracle \( B_{\Omega} \) to be re-expressed by \( B_{\Omega} \), and the modification \( \log \frac{T'}{\pi'} \), which makes the motivation in Equation 4 practical.

**R(A)w(T)m(\( \Omega = 1 \))** If we introduce the variational distribution \( p^\pi_{\Omega} (\tau) := p(s_0) \prod_{t=1}^T T'(s_{t+1} | s_t, a_t) \pi(a_t | s_t) \), we can recover the weighted-regression-style \([\text{Wang et al., 2020; Peng et al., 2019; Abdolmaleki et al., 2018; Peters et al., 2010} \] objective by maximizing \( J(\pi', \pi) := \mathbb{E}_{\tau \sim p^\pi_{\Omega} (\tau)} \left[ \sum_{t=0}^\infty \gamma^t \left( r_t - \eta \log \frac{T'(s_{t+1} | s_t, a_t)}{\pi(s_t | s_t, a_t)} - \eta \log \frac{T'(s' | s, a)}{\pi'(s' | s, a)} \right) \right] \) lower bound of \( \log p^\pi_{\Omega} (\Omega = 1) \). Following the Expectation Maximization (EM) algorithm, we can maximize \( J(\pi', \pi) \) by iteratively (E-step) improving \( J(\pi', \cdot) \) w.r.t. \( \pi' \) and (M-step) updating \( \pi \) w.r.t. \( \pi' \).

(E-step) We define \( \hat{Q}(s, a, s') = \mathbb{E}_{\tau \sim p^\pi_{\Omega} (\tau)} \left[ \sum_t \gamma^t \log \frac{T'(s' | s, a)}{T(s' | s, a)} \right] \). Then, given offline data \( D' \), we can rewrite \( J(\pi', \pi) \) as a constrained objective \([\text{Abdolmaleki et al., 2018}] \):

\[
\max_{\hat{Q}} \mathbb{E}_{d_{D'}(s, a) \sim p^\pi_{\Omega} (\tau)} \left[ Q(s, a) - \eta \hat{Q}(s, a, s') \right], \text{ s.t. } \mathbb{E}_{d_{D'}(s, a) \sim p^\pi_{\Omega} (\tau)} \left[ D_{KL} (\pi'(a | s) | | \pi(a | s)) \right] \leq \epsilon.
\]

When considering a fixed \( \pi \), the above optimization over \( \pi' \) can be solved analytically \([\text{Vieillard et al., 2020; Geist et al., 2019; Peng et al., 2019}] \). The optimal \( \pi'_* \) is then given by \( \pi'_*(a | s) \propto \pi(a | s) \exp \left( Q'(s, a) \right) \). As the policy evaluation in Equation 1 (Footnote 2), we estimate \( Q(s, a) \) and \( Q(s, a, s') \) by minimizing the Bellman error with offline samples in \( D' \).

(M-step) Then, we can project \( \pi'_* \) onto the manifold of the parameterized \( \pi \):

\[
\arg \min_\pi \mathbb{E}_{d_{D'}(s, a) \sim p^\pi_{\Omega} (\tau)} \left[ D_{KL} \left( \pi'_*(a | s) | | \pi(a | s) \right) \right]
= \arg \max_\pi \mathbb{E}_{s, a, s' \sim D'} \left[ \log \pi(a | s) \exp \left( Q(s, a) \right) \exp \left( -\eta \hat{Q}(s, a, s') \right) \right].
\]

(8)

From the regression view, prior work MPO \([\text{Abdolmaleki et al., 2018}] \) infers actions with Q-value weighted regression, progressive approach compared to behavior cloning; however, such paradigm lacks the ability to capture transition dynamics. We explicitly introduce the \( -\eta \hat{Q}(s, a, s') \) term, which as we show in experiments, is a crucial component for eliminating the dynamics shift.

**Implementation:** In practice, we adopt offline samples in \( D \) to approximate the true dynamics \( T \). of \( M \), and introduce a pair of binary classifiers, \( q_{\text{obs}}(\cdot | s, a, s') \) and \( q_{\text{act}}(\cdot | s, a) \), to replace \( \log \frac{T'(s' | s, a)}{T(s' | s, a)} \) as in \([\text{Eysenbach et al., 2021}] \): 

\[
T'(s' | s, a) = \log \frac{q_{\text{obs}}(s', a | s, a)}{q_{\text{act}}(s' | s, a)} - \log \frac{q_{\text{obs}}(s, a | s, a)}{q_{\text{act}}(s | s, a)}.
\]

(See Appendix A.1.3 for details). Although the amount of data \( D \) sampled from the target \( M \) is reduced in our problem setup, we experimentally find that such classifiers are sufficient to achieve good performance.
5.2 Dynamics-Aware Reward Augmentation in Model-based Formulation

Following Equation [3] we then characterize the dynamics shift compensation term as in the above model-free analysis in the model-based offline formulation. We will find that across different derivations, our reward augmentation \( \Delta r \) has always maintained the functional consistency and simplicity.

Following MOPO, we assume \( F = \{ f : \|f\|_\infty \leq 1 \} \), then we have \( d_F(\mathcal{T}'(s'|s,a), \hat{\mathcal{T}}(s'|s,a)) = D_{TV}(\mathcal{T}'(s'|s,a), \hat{\mathcal{T}}(s'|s,a)) \leq (D_{KL}(\mathcal{T}'(s'|s,a), \hat{\mathcal{T}}(s'|s,a))/2)^2 \), where \( D_{TV} \) is the total variance distance. Then we introduce the admissible error \( u(s,a) \) such that \( d_F(\hat{\mathcal{T}}(s'|s,a), \mathcal{T}(s'|s,a)) \leq u(s,a) \) for all \((s,a)\), and \( \eta \) and \( \delta \) such that \( (D_{KL}(\hat{\mathcal{T}}, \mathcal{T})/2)^2 \leq \eta D_{KL}(\hat{\mathcal{T}}, \mathcal{T}) + \delta \). Following Lemma 3, we thus can maximize the following lower bound with the samples in \( M' \) (\( \lambda := \frac{\eta \lambda^{u \lambda}}{1-\gamma} \)):

\[
\eta M(\pi) \geq \mathbb{E}_{s,a,s' \sim \hat{d}_{M'}}(s|\pi(s|a),\Delta r(s'|s,a)) \left[ r(s,a) - \eta \lambda \log \frac{\mathcal{T}'(s'|s,a)}{\hat{\mathcal{T}}(s'|s,a)} - \lambda u(s,a) - \lambda \delta \right].
\]  

**Implementation:** We model the dynamics \( \hat{\mathcal{T}} \) and \( \mathcal{T} \) with an ensemble of \( 2^N \) parameterized Gaussian distributions: \( \mathcal{N}_\mu^{\mathbf{s}}(\mu(s,a), \Sigma_{\mathbf{s}}(s,a)) \) and \( \mathcal{N}_\mu^{\mathbf{d}}(\mu(s,a), \Sigma_{\mathbf{d}}(s,a)) \), where \( i \in [1, N] \). We approximate \( u \) with the maximum standard deviation of the learned models in the ensemble: \( u(s,a) = \max_{i=1}^N \| \Sigma_{\mathbf{s}}(s,a) \|_F \), omit the training-independent \( \delta \), and treat \( \lambda \) as a hyperparameter as in MOPO. For the log \( \frac{\mathcal{T}'}{\hat{\mathcal{T}}} \) term, we resort to the above classifiers \((\delta_{\mathbf{ss}}, \delta_{\mathbf{sd}})\) in model-free setting. (See Appendix A.3.2 for comparison between using classifiers and estimated-dynamics ratio.)

6 Experiments

We present empirical demonstrations of our dynamics-aware reward augmentation (DARA) in a variety of settings. We start with two simple control experiments that illustrate the significance of DARA under the domain (dynamics) adaptation setting. Then we incorporate DARA into state-of-the-art (model-free and model-based) offline RL methods and evaluate the performance on the D4RL tasks. Finally, we compare our framework to several cross-domain-based baselines on simulated and real-world tasks. Note that for the dynamics adaptation, we also release a (source) dataset as a complement to D4RL, along with the quadruped robot dataset in simulator (source) and real (target).

6.1 How does DARA handle the dynamics shift in offline setting?

Figure 2: External dynamics shift: (left) source and target MDPs (target contains an obstacle represented with the dashed line); (middle) top plots (w/o Aug.) depict the trajectories that are generated by the learned policy with vanilla MPO; (middle) bottom plots (DARA) depict the trajectories that are generated by the learned policy with DARA-based MPO; (right) learned Q-values on the state-action pairs in left subfigue.

Here we characterize both external and internal dynamics shifts: In Map tasks (Figure 2 [left]), the source dataset \( D' \) is collected in a 2D map and the target \( D \) is collected in the same environment but with an obstacle (the dashed line); In Ant tasks (Figure 3 [left]), the source dataset \( D' \) is collected using the Mujoco Ant and the target \( D \) is collected with the same Ant but one joint of which is restricted.

Using MPO, as an example of offline RL method, we train a policy on dataset \( \{D' \cup D\} \) and deploy the acquired policy in both source and target MDPs. As shown in Figure 2 (middle-top, w/o Aug.), such training paradigm does not produce an adaptive policy for the target. By modifying rewards in...
Table 1: Normalized scores for the (target) D4RL tasks, where our results are averaged over 5 seeds. The arrows in each four-tuple indicate whether the current performance has improved (↑) or not (↓) compared to the previous value. If 1T+10S DARA achieves comparable (less than 10% degradation) or better performance compared to baseline 1T, we highlight our scores in bold (in each four-tuple).

| Body Mass Shift | 10T | 1T | 1T+10S w/o Aug. | 1T+10S DARA | 10T | 1T | 1T+10S w/o Aug. | 1T+10S DARA | 10T | 1T | 1T+10S w/o Aug. | 1T+10S DARA |
|-----------------|-----|----|-----------------|-------------|-----|----|-----------------|-------------|-----|----|-----------------|-------------|
|                  | BEAR | BRAC-p | AWR | BCQ | CQL | MOPO | BEAR | BRAC-p | AWR | BCQ | CQL | MOPO |
| Random           | 11.4 | 1.0 | 4.6 | 8.4 | 11.0 | 10.9 | 9.6 | 11.0 | 10.2 | 10.3 | 3.4 | 4.5 |
| Medium           | 52.1 | 0.8 | 0.9 | 1.6 | 32.7 | 29.0 | 29.2 | 32.9 | 35.9 | 30.9 | 20.8 | 28.9 |
| Medium-R         | 33.7 | 1.3 | 18.2 | 34.1 | 0.6 | 5.4 | 20.1 | 30.8 | 28.4 | 8.8 | 4.1 | 4.2 |
| Medium-E         | 96.3 | 0.8 | 0.6 | 1.2 | 1.9 | 34.5 | 32.3 | 34.7 | 27.1 | 27.0 | 26.8 | 26.6 |
| Hopper           | 10.6 | 10.6 | 8.3 | 9.7 | 10.8 | 10.4 | 10.2 | 10.4 | 11.7 | 4.8 | 2.0 | 2.1 |
| Medium           | 54.5 | 37.1 | 25.7 | 38.4 | 58.0 | 43.0 | 44.9 | 59.3 | 28.0 | 4.1 | 5.0 | 10.7 |
| Medium-R         | 33.1 | 9.3 | 28.7 | 32.8 | 48.6 | 9.6 | 1.4 | 3.7 | 67.5 | 10.0 | 5.5 | 8.4 |
| Medium-E         | 110.9 | 58 | 75.4 | 84.2 | 98.7 | 59.7 | 53.6 | 99.7 | 23.7 | 1.6 | 4.8 | 5.8 |
| Walker2d         | 7.3 | 1.5 | 3.1 | 3.2 | -0.2 | 0.0 | 1.3 | 3.2 | 1.5 | 1.3 | 2.0 | 2.4 |
| Medium           | 59.1 | -0.5 | 0.6 | 0.3 | 77.5 | 64.4 | 70.0 | 78.0 | 17.4 | 14.8 | 17.1 | 12.2 |
| Medium-R         | 19.2 | 0.7 | 6.5 | 7.3 | -0.3 | 8.5 | 9.9 | 18.6 | 15.5 | 7.4 | 1.6 | 1.5 |
| Medium-E         | 40.1 | -0.1 | 1.5 | 2.3 | 76.9 | 20.6 | 64.1 | 77.5 | 53.8 | 35.5 | 52.5 | 53.3 |
|                  | BCQ | CQL | MOPO | BCQ | CQL | MOPO | BCQ | CQL | MOPO | BCQ | CQL | MOPO |
| Walker2d         | 4.9 | 1.8 | 4.5 | 4.8 | 7.0 | 1.7 | 3.2 | 3.4 | 13.6 | -0.2 | -0.1 | -0.1 |
| Medium           | 53.1 | 32.8 | 50.9 | 52.3 | 79.2 | 42.9 | 80.0 | 81.7 | 17.8 | 7.0 | 5.7 | 11.0 |
| Medium-R         | 15.0 | 6.9 | 14.9 | 15.1 | 26.7 | 4.6 | 0.8 | 2.0 | 39.0 | 5.1 | 3.1 | 14.2 |
| Medium-E         | 57.5 | 32.5 | 55.2 | 57.2 | 111.0 | 49.5 | 63.5 | 93.3 | 44.6 | 5.3 | 5.5 | 17.2 |

source \(D'\), we show that applying the same training paradigm on the reward augmented data exhibits a positive transfer ability in Figure 2(middle-bottom, DARA). In Figure 2(right), we show that our DARA produces low Q-values on the obstructive state-action pairs (in left) compared to the vanilla DARA, or better performance compared to baseline adaptation with reward modifications, e.g., think of DARA as finding out these transitions that exhibit dynamics shifts and enabling dynamics that are beyond reach in target and yet are high valued, would yield a negative transfer. Thus, we can produce a penalty (red slices) on these state-action pairs (in source) that produce infeasible next-state-action pairs (in target). Incorporating our reward augmentation, we observe that compared to 1T and 1T+10S w/o Aug., that both use 10% of the target offline data, our 1T+10S DARA significantly improves the performance across a majority of tasks. Moreover, DARA can achieve comparable or better performance compared to baseline 10T that training with ten times as much target offline data.
Table 2: Normalized scores in (target) D4RL tasks, where "Tune" denotes baseline "fine-tune". We observe that with same amount (10%) of target offline data, DARA greatly outperforms baselines.

| Body Mass Shift | Tune | DARA | Tune | DARA | Tune | DARA | Tune | DARA | π_π^T + Tπ_p |
|-----------------|------|------|------|------|------|------|------|------|----------------|
| **Hopper**      |      |      |      |      |      |      |      |      |                |
| Random          | 0.8  | 8.4↑ | 6.0  | 11.0↑| 8.8  | 9.7↑ | 31.6 | 10.4↓| 0.7  | 2.1↑ | 10.6 | 9.0          |
| Medium          | 0.8  | 1.6↑ | 22.7 | 32.9↑| 31.7 | 38.4↑| 44.5 | 59.3↑| 0.7  | 10.7↑ | 48.8 | 23.1         |
| Medium-R        | 0.7  | 34.1↑| 14.7 | 30.8↑| 27.5 | 32.8↑| 1.3  | 3.7↑ | 0.6  | 8.4↑ | 17.1 | 20.4         |
| Medium-E        | 0.9  | 1.2↑ | 19.2 | 34.7↑| 85.9 | 84.2↑| 47.6 | 99.7↑| 2.2  | 5.8↑ | 28.1 | 38.9         |
| **Walker2d**    |      |      |      |      |      |      |      |      |                |
| Random          | 6.6  | 3.2↓ | 3.9  | 3.2↓ | 4.7  | 4.8↑ | 1.1  | 3.4↑ | 0.1  | -0.1↓ | 6.0  | -0.2         |
| Medium          | 0.3  | 76.0 | 78.0 | 28.4 | 52.3 | 72.3 | 81.7↑| -0.2 | 11.0↑ | 30.1 | 56.7         |
| Medium-R        | 1.2  | 7.3↑ | 10.0 | 18.6↑| 10.4 | 15.1↑| 1.8  | 2.0↑ | 0.0  | 14.2↑ | 13.3 | 12.5         |
| Medium-E        | 2.4  | 2.3↓ | 74.5 | 77.5↑| 22.7 | 57.2↑| 68.6 | 93.3↑| 7.3  | 17.2↑ | 43.7 | 82.7         |

6.3 Can DARA perform better than cross-domain baselines?

In Section 6.2, 1T+10S w/o Aug. does not explicitly learn policy for the target dynamics, thus one proposal (1T+10S fine-tune) for adapting the target dynamics is fine-tuning the model that learned with source offline data, using the (reduced) target offline data. Moreover, we also compare DARA with the recently proposed MABE (Cang et al., 2021), which is suitable well for our cross-dynamics setting by introducing behavioral priors π_p in the model-based offline setting. Thus, we implement two baselines, 1) 1T+10S MABE π_pT and 2) 1T+10S MABE Tπ_p, which denote 1) learning π_p with target domain data and T with source domain data, and 2) learning π_p with source domain data and T with target domain data, respectively. We show the results for the Walker (with body mass shift) in Table 3 and more experiments in Appendix [A.3.2]. Our results show that DARA achieves significantly better performance than the naive fine-tune-based approaches in a majority of tasks (67 “↑” vs. 13 “↓”), including results in appendix). On twelve out of the sixteen tasks (including results in appendix), DARA-based methods outperform the MABE-based methods. We attribute MABE’s failure to the difficulty of the reduced target offline data, which limits the generalization of the learned π_p or T under such data. However, such reduced data (10% of target) is sufficient to modify rewards in the source offline data, which thus encourages better performance for our DARA.

For real-world tasks, we also test DARA in a new offline dataset on the quadruped robot (see appendix for details). Note that we cannot access the privileged information (e.g., coordinate) in real robot, thus the target offline data (collected in real-world) does not contain rewards. This means that prior fine-tune-based and MABE-based methods become unavailable. However, our reward augmentation frees us from the requisite of rewards in target domain. We can freely perform offline training only using the augmented source offline data as long as the learned Δp is sufficient. For comparison, we also employ a baseline (w/o Aug.); directly deploying the learned policy with source data into the (target) real-world. We present the results (deployed in real with obstructive stairs) in Table 3 and videos in supplementary material. We can observe that training with our reward augmentation, the performance can be substantially improved. Due to page limit, we refer readers to Appendix [A.3.6] for more experimental results and discussion.

7 Conclusion

In this paper, we formulate the dynamics shift in offline RL. Based on prior model-based and model-free offline algorithms, we propose the dynamics-aware reward augmentation (DARA) framework that characterizes constraints over state-action-next-state distributions. Empirically we demonstrate DARA can eliminate the dynamics shift and outperform baselines in simulated and real-world tasks.

In Appendix [A.2], we characterize our dynamics-aware reward augmentation from the density regularization view, which shows that it is straightforward to derive the reward modification built on prior regularized max-return objective e.g., AlgaeDICE (Nachum et al., 2019b). We list some related works in Table 4, where the majority of the existing work focuses on regularizing state-action distribution, while dynamics shift receives relatively little attention. Thus, we hope to shift the focus of the community towards analyzing how dynamics shift affects RL and how to eliminate the effect.
REPRODUCIBILITY STATEMENT

Our experimental evaluation is conducted with publicly available D4RL (Fu et al., 2020) and NeoRL (Qin et al., 2021). In Appendix A.4 and A.5 we provide the environmental details and training setup for our real-world sim2real tasks. In supplementary material, we upload our source code and the collected offline dataset for the the quadruped robot.

ACKNOWLEDGMENTS

We thank Zifeng Zhuang, Yachen Kang and Qiangxing Tian for helpful feedback and discussions. This work is supported by NSFC General Program (62176215).

REFERENCES

Abbas Abdolmaleki, Jost Tobias Springenberg, Yuval Tassa, Rémi Munos, Nicolas Heess, and Martin A. Riedmiller. Maximum a posteriori policy optimisation. In 6th International Conference on Learning Representations, ICLR 2018, Vancouver, BC, Canada, April 30 - May 3, 2018, Conference Track Proceedings. OpenReview.net, 2018.

Philip J. Ball, Cong Lu, Jack Parker-Holder, and Stephen J. Roberts. Augmented world models facilitate zero-shot dynamics generalization from a single offline environment. In Marina Meila and Tong Zhang (eds.), Proceedings of the 38th International Conference on Machine Learning, ICML 2021, 18-24 July 2021, Virtual Event, volume 139 of Proceedings of Machine Learning Research, pp. 619–629. PMLR, 2021.

Catherine Cang, Aravind Rajeswaran, Pieter Abbeel, and Michael Laskin. Behavioral priors and dynamics models: Improving performance and domain transfer in offline RL. CoRR, abs/2106.09119, 2021. URL https://arxiv.org/abs/2106.09119

Yevgen Chebotar, Karol Hausman, Yao Lu, Ted Xiao, Dmitry Kalashnikov, Jacob Varley, Alex Irpan, Benjamin Eysenbach, Ryan Julian, Chelsea Finn, and Sergey Levine. Actionable models: Unsupervised offline reinforcement learning of robotic skills. In Marina Meila and Tong Zhang (eds.), Proceedings of the 38th International Conference on Machine Learning, ICML 2021, 18-24 July 2021, Virtual Event, volume 139 of Proceedings of Machine Learning Research, pp. 1518–1528. PMLR, 2021. URL http://proceedings.mlr.press/v139/chebotar21a.html

Jinglin Chen and Nan Jiang. Information-theoretic considerations in batch reinforcement learning. In Kamalika Chaudhuri and Ruslan Salakhutdinov (eds.), Proceedings of the 36th International Conference on Machine Learning, ICML 2019, 9-15 June 2019, Long Beach, California, USA, volume 97 of Proceedings of Machine Learning Research, pp. 1042–1051. PMLR, 2019.

Xinyue Chen, Zijian Zhou, Zheng Wang, Che Wang, Yanqiu Wu, and Keith Ross. Bail: Best-action imitation learning for batch deep reinforcement learning. arXiv preprint arXiv:1910.12179, 2019.

Erwin Coumans and Yunfei Bai. Pybullet, a python module for physics simulation for games, robotics and machine learning. http://pybullet.org 2016–2021.

Benjamin Eysenbach and Sergey Levine. If maxent RL is the answer, what is the question? CoRR, abs/1910.01913, 2019. URL http://arxiv.org/abs/1910.01913

Benjamin Eysenbach, Shreyas Chaudhari, Swapnil Asawa, Sergey Levine, and Ruslan Salakhutdinov. Off-dynamics reinforcement learning: Training for transfer with domain classifiers. In 9th International Conference on Learning Representations, ICLR 2021, Virtual Event, Austria, May 3-7, 2021. OpenReview.net, 2021.

Justin Fu, Aviral Kumar, Ofir Nachum, George Tucker, and Sergey Levine. D4RL: datasets for deep data-driven reinforcement learning. CoRR, abs/2004.07219, 2020. URL http://arxiv.org/abs/2004.07219
Scott Fujimoto, David Meger, and Doina Precup. Off-policy deep reinforcement learning without 
exploration. In Kamalika Chaudhuri and Ruslan Salakhutdinov (eds.), *Proceedings of the 36th 
International Conference on Machine Learning*, ICML 2019, 9-15 June 2019, Long Beach, Cali-
ifornia, USA, volume 97 of *Proceedings of Machine Learning Research*, pp. 2052–2062. PMLR, 
2019.

Matthieu Geist, Bruno Scherrer, and Olivier Pietquin. A theory of regularized markov decision 
processes. In Kamalika Chaudhuri and Ruslan Salakhutdinov (eds.), *Proceedings of the 36th 
International Conference on Machine Learning*, ICML 2019, 9-15 June 2019, Long Beach, Cali-
ifornia, USA, volume 97 of *Proceedings of Machine Learning Research*, pp. 2160–2169. PMLR, 
2019.

Seyed Kamyar Seyed Ghasemipour, Dale Schuurmans, and Shixiang Shane Gu. Emaq: Expected-
max q-learning operator for simple yet effective offline and online RL. In Marina Meila and Tong 
Zhang (eds.), *Proceedings of the 38th International Conference on Machine Learning*, ICML 
2021, 18-24 July 2021, Virtual Event, volume 139 of *Proceedings of Machine Learning Research*, 
pp. 3682–3691. PMLR, 2021.

Tuomas Haarnoja, Aurick Zhou, Kristian Hartikainen, George Tucker, Sehoon Ha, Jie Tan, Vikash 
Kumar, Henry Zhu, Abhishek Gupta, Pieter Abbeel, and Sergey Levine. Soft actor-critic al-
gorithms and applications. *CoRR*, abs/1812.05905, 2018. URL http://arxiv.org/abs/
1812.05905

Behzad Haghgoo, Allan Zhou, Archit Sharma, and Chelsea Finn. Discriminator augmented model-
based reinforcement learning. *CoRR*, abs/2103.12999, 2021. URL https://arxiv.org/
abs/2103.12999

Atil Iscen, Ken Caluwaerts, Jie Tan, Tingnan Zhang, Erwin Coumans, Vikas Sindhwani, and 
Vincent Vanhoucke. Policies modulating trajectory generators. In 2nd Annual Conference 
on Robot Learning, *CoRL* 2018, Zürich, Switzerland, 29-31 October 2018, Proceedings, vol-
ume 87 of *Proceedings of Machine Learning Research*, pp. 916–926. PMLR, 2018. URL 
http://proceedings.mlr.press/v87/iscen18a.html

Nan Jiang and Jiawei Huang. Minimax value interval for off-policy evaluation and policy op-
timization. In Hugo Larochelle, Marc’Aurelio Ranzato, Raia Hadsell, Maria-Florina Balcan, 
and Hsuan-Tien Lin (eds.), *Advances in Neural Information Processing Systems 33: Annual 
Conference on Neural Information Processing Systems 2020, NeurIPS 2020, December 6-12, 
2020, virtual*, 2020. URL https://proceedings.neurips.cc/paper/2020/hash/
1cd138d0499a68f4bb72bee04bbec2d7-Abstract.html

Rahul Kidambi, Aravind Rajeswaran, Praneeth Netrapalli, and Thorsten Joachims. Morel: Model-
based offline reinforcement learning. In Hugo Larochelle, Marc’Aurelio Ranzato, Raia Hadsell, 
Maria-Florina Balcan, and Hsuan-Tien Lin (eds.), *Advances in Neural Information Processing 
Systems 33: Annual Conference on Neural Information Processing Systems 2020, NeurIPS 2020, 
December 6-12, 2020*, virtual, 2020.

Ilya Kostrikov, Rob Fergus, Jonathan Tompson, and Ofir Nachum. Offline reinforcement learning 
with fisher divergence critic regularization. In Marina Meila and Tong Zhang (eds.), *Proceedings 
of the 38th International Conference on Machine Learning*, ICML 2021, 18-24 July 2021, Virtual 
Event, volume 139 of *Proceedings of Machine Learning Research*, pp. 5774–5783. PMLR, 2021.

Aviral Kumar, Justin Fu, Matthew Soh, George Tucker, and Sergey Levine. Stabilizing off-policy 
q-learning via bootstrapping error reduction. In Hanna M. Wallach, Hugo Larochelle, Alina 
Beygelzimer, Florence d’Alché-Buc, Emily B. Fox, and Roman Garnett (eds.), *Advances in Neu-
ral Information Processing Systems 32: Annual Conference on Neural Information Processing 
Systems 2019, NeurIPS 2019, December 8-14, 2019, Vancouver, BC, Canada*, pp. 11761–11771, 
2019.

Aviral Kumar, Aurick Zhou, George Tucker, and Sergey Levine. Conservative q-learning for offline 
reinforcement learning. In Hugo Larochelle, Marc’Aurelio Ranzato, Raia Hadsell, Maria-Florina 
Balcan, and Hsuan-Tien Lin (eds.), *Advances in Neural Information Processing Systems 33: An-
nual Conference on Neural Information Processing Systems 2020, NeurIPS 2020, December 6-12, 
2020*, virtual, 2020a.
Saurabh Kumar, Aviral Kumar, Sergey Levine, and Chelsea Finn. One solution is not all you need: Few-shot extrapolation via structured maxent RL. In Hugo Larochelle, Marc’Aurelio Ranzato, Raia Hadsell, Maria-Florina Balcan, and Hsuan-Tien Lin (eds.), Advances in Neural Information Processing Systems 33: Annual Conference on Neural Information Processing Systems 2020, NeurIPS 2020, December 6-12, 2020, virtual, 2020b. URL https://proceedings.neurips.cc/paper/2020/hash/5d151d1059a6281335a10732fc49620e-Abstract.html

Sascha Lange, Thomas Gabel, and Martin Riedmiller. Batch reinforcement learning. In Reinforcement learning, pp. 45–73. Springer, 2012.

Joonho Lee, Jemin Hwangbo, Lorenz Wellhausen, Vladlen Koltun, and Marco Hutter. Learning quadrupedal locomotion over challenging terrain. Science Robotics, 5(47), 2020. doi: 10.1126/scirobotics.abc5986. URL https://robotics.sciencemag.org/content/5/47/eabc5986

Sergey Levine. Reinforcement learning and control as probabilistic inference: Tutorial and review. CoRR, abs/1805.00909, 2018. URL http://arxiv.org/abs/1805.00909

Sergey Levine, Aviral Kumar, George Tucker, and Justin Fu. Offline reinforcement learning: Tutorial, review, and perspectives on open problems. CoRR, abs/2005.01643, 2020. URL https://arxiv.org/abs/2005.01643

Jinxin Liu, Hao Shen, Donglin Wang, Yachen Kang, and Qiangxing Tian. Unsupervised domain adaptation with dynamics-aware rewards in reinforcement learning. Advances in Neural Information Processing Systems, 34, 2021.

Qiang Liu, Lihong Li, Ziyang Tang, and Dengyong Zhou. Breaking the curse of horizon: Infinite-horizon off-policy estimation. pp. 5361–5371, 2018. URL https://proceedings.neurips.cc/paper/2018/hash/dda04f9d634145a9c68d5dfe53b21272-Abstract.html

Eric Mitchell, Rafael Rafailov, Xue Bin Peng, Sergey Levine, and Chelsea Finn. Offline meta-reinforcement learning with advantage weighting. In Marina Meila and Tong Zhang (eds.), Proceedings of the 38th International Conference on Machine Learning, ICML 2021, 18-24 July 2021, Virtual Event, volume 139 of Proceedings of Machine Learning Research, pp. 7780–7791. PMLR, 2021.

Ofir Nachum and Bo Dai. Reinforcement learning via fenchel-rockafellar duality. CoRR, abs/2001.01866, 2020. URL http://arxiv.org/abs/2001.01866

Ofir Nachum, Yinlam Chow, Bo Dai, and Lihong Li. Dualdice: Behavior-agnostic estimation of discounted stationary distribution corrections. arXiv preprint arXiv:1906.04733, 2019a.

Ofir Nachum, Bo Dai, Ilya Kostrikov, Yinlam Chow, Lihong Li, and Dale Schuurmans. Algae_dice: Policy gradient from arbitrary experience. CoRR, abs/1912.02074, 2019b. URL http://arxiv.org/abs/1912.02074

Ashvin Nair, Murtaza Dalal, Abhishek Gupta, and Sergey Levine. Accelerating online reinforcement learning with offline datasets. CoRR, abs/2006.09359, 2020. URL https://arxiv.org/abs/2006.09359

Sinno Jialin Pan and Qiang Yang. A survey on transfer learning. IEEE Trans. Knowl. Data Eng., 22 (10):1345–1359, 2010. doi: 10.1109/TKDE.2009.191. URL https://doi.org/10.1109/TKDE.2009.191

Xue Bin Peng, Marcin Andrychowicz, Wojciech Zaremba, and Pieter Abbeel. Sim-to-real transfer of robotic control with dynamics randomization. In 2018 IEEE International Conference on Robotics and Automation, ICRA 2018, Brisbane, Australia, May 21-25, 2018, pp. 1–8. IEEE, 2018. doi: 10.1109/ICRA.2018.8460528. URL https://doi.org/10.1109/ICRA.2018.8460528
Xue Bin Peng, Aviral Kumar, Grace Zhang, and Sergey Levine. Advantage-weighted regression: Simple and scalable off-policy reinforcement learning. CoRR, abs/1910.00177, 2019. URL http://arxiv.org/abs/1910.00177

Jan Peters, Katharina Mulling, and Yasemin Altun. Relative entropy policy search. In Twenty-Fourth AAAI Conference on Artificial Intelligence, 2010.

Rongjun Qin, Songyi Gao, Xingyuan Zhang, Zhen Xu, Shengkai Huang, Zewan Li, Weinan Zhang, and Yang Yu. Neorl: A near real-world benchmark for offline reinforcement learning. arXiv preprint arXiv:2102.00714, 2021.

Y. Sakakibara, K. Kan, Y. Hosoda, M. Hattori, and M. Fujie. Foot trajectory for a quadruped walking machine. In IEEE International Workshop on Intelligent Robots and Systems, Towards a New Frontier of Applications, pp. 315–322 vol.1, 1990. doi: 10.1109/IROS.1990.262407.

Noah Y Siegel, Jost Tobias Springenberg, Felix Berkenkamp, Abbas Abdolmaleki, Michael Neunert, Thomas Lampe, Roland Hafner, Nicolas Heess, and Martin Riedmiller. Keep doing what worked: Behavioral modelling priors for offline reinforcement learning. arXiv preprint arXiv:2002.08396, 2020.

Richard S. Sutton. Integrated architectures for learning, planning, and reacting based on approximating dynamic programming. In Bruce W. Porter and Raymond J. Mooney (eds.), Machine Learning, Proceedings of the Seventh International Conference on Machine Learning, Austin, Texas, USA, June 21-23, 1990, pp. 216–224. Morgan Kaufmann, 1990. doi: 10.1016/b978-1-55860-141-3.50030-4.

Josh Tobin, Rachel Fong, Alex Ray, Jonas Schneider, Wojciech Zaremba, and Pieter Abbeel. Domain randomization for transferring deep neural networks from simulation to the real world. 2017.

Masatoshi Uehara, Jiawei Huang, and Nan Jiang. Minimax weight and q-function learning for off-policy evaluation. In Proceedings of the 37th International Conference on Machine Learning, ICML 2020, 13-18 July 2020, Virtual Event, volume 119 of Proceedings of Machine Learning Research, pp. 9659–9668. PMLR, 2020. URL http://proceedings.mlr.press/v119/uehara20a.html.

Nino Vieillard, Tadashi Kozuno, Bruno Scherrer, Olivier Pietquin, Rémi Munos, and Matthieu Geist. Leverage the average: an analysis of KL regularization in reinforcement learning. In Hugo Larochelle, Marc'Aurelio Ranzato, Raia Hadsell, Maria-Florina Balcan, and Hsuan-Tien Lin (eds.), Advances in Neural Information Processing Systems 33: Annual Conference on Neural Information Processing Systems 2020, NeurIPS 2020, December 6-12, 2020, virtual, 2020.

Xingxing Wang. Unitree robotics. https://www.unitree.com/products/a1 2020.

Ziyu Wang, Alexander Novikov, Konrad Zolna, Jost Tobias Springenberg, Scott Reed, Bobak Shahriari, Noah Siegel, Josh Merel, Caglar Gulcehre, Nicolas Heess, et al. Critic regularized regression. arXiv preprint arXiv:2006.15134, 2020.

Yifan Wu, George Tucker, and Ofir Nachum. Behavior regularized offline reinforcement learning. CoRR, abs/1911.11361, 2019. URL http://arxiv.org/abs/1911.11361

Haoran Xu, Xianyuan Zhan, and Xiangyu Zhu. Constraints penalized q-learning for safe offline reinforcement learning. CoRR, abs/2107.09003, 2021. URL https://arxiv.org/abs/2107.09003

Mengjiao Yang, Ofir Nachum, Bo Dai, Lihong Li, and Dale Schuurmans. Off-policy evaluation via the regularized lagrangian. In Hugo Larochelle, Marc’Aurelio Ranzato, Raia Hadsell, Maria-Florina Balcan, and Hsuan-Tien Lin (eds.), Advances in Neural Information Processing Systems 33: Annual Conference on Neural Information Processing Systems 2020, NeurIPS 2020, December 6-12, 2020, virtual, 2020. URL https://proceedings.neurips.cc/paper/2020/hash/488e4104520c6aab692863cc1dba45af-Abstract.html.
Tianhe Yu, Garrett Thomas, Lantao Yu, Stefano Ermon, James Y. Zou, Sergey Levine, Chelsea Finn, and Tengyu Ma. MOPO: model-based offline policy optimization. In Hugo Larochelle, Marc'Aurelio Ranzato, Raia Hadsell, Maria-Florina Balcan, and Hsuan-Tien Lin (eds.), Advances in Neural Information Processing Systems 33: Annual Conference on Neural Information Processing Systems 2020, NeurIPS 2020, December 6-12, 2020, virtual, 2020.

Tianhe Yu, Aviral Kumar, Rafael Rafailov, Aravind Rajeswaran, Sergey Levine, and Chelsea Finn. COMBO: conservative offline model-based policy optimization. *CoRR*, abs/2102.08363, 2021. URL [https://arxiv.org/abs/2102.08363](https://arxiv.org/abs/2102.08363).

Hongyin Zhang, Jilong Wang, Zhengqing Wu, Yinuo Wang, and Donglin Wang. Terrain-aware risk-assessment-network-aided deep reinforcement learning for quadrupedal locomotion in tough terrain. In 2021 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), pp. 4538–4545. IEEE.

Ruiyi Zhang, Bo Dai, Lihong Li, and Dale Schuurmans. Gendice: Generalized offline estimation of stationary values. In 8th International Conference on Learning Representations, ICLR 2020, Addis Ababa, Ethiopia, April 26-30, 2020. OpenReview.net, 2020. URL [https://openreview.net/forum?id=HkxlcnVFwB](https://openreview.net/forum?id=HkxlcnVFwB).
# Appendix

## A.1 Derivation

### A.1.1 Proof of Lemma 3

Let $B_M^\pi V(s) = \mathbb{E}_{a \sim \pi(a|s)} [r(s, a) + \gamma s' \sim T(s'|s,a) [V(s')]]$ and $r(s) = \mathbb{E}_{a \sim \pi(a|s)} [r(s, a)]$. Then, we have

$$
\eta_M(\pi) - \eta_M(\pi) = \mathbb{E}_{s_0 \sim \rho_0(s)} \left[ V_M(s_0) - V_M(s_0) \right]
= \sum_{t=0}^{\infty} \gamma^t \mathbb{E}_{s_t \sim P(s_t|\pi, M', t)} \mathbb{E}_{a_t \sim \pi(a_t|s_t)} [r(s_t, a_t) - \mathbb{E}_{s_{t+1} \sim \rho_0(s)} [V_M(s_t)]]
= \sum_{t=0}^{\infty} \gamma^t \mathbb{E}_{s_t \sim P(s_t|\pi, M', t)} \left[ r(s_t) + V_M(s_t) - V_M(s_t) \right] - \mathbb{E}_{s_{t+1} \sim \rho_0(s)} [V_M(s_t)]
= \sum_{t=0}^{\infty} \gamma^t \mathbb{E}_{s_t \sim P(s_t|\pi, M', t)} \left[ r(s_t) + \gamma V_M(s_{t+1}) - V_M(s_t) \right]
= \sum_{t=0}^{\infty} \gamma^t \mathbb{E}_{s_t \sim P(s_t|\pi, M', t)} \left[ r(s_t) + \gamma V_M(s_{t+1}) - r(s_t) + \gamma \mathbb{E}_{a_t \sim \pi(a|s_t)} [V_M(s_t)] \right]
= \mathbb{E}_{s_0 \sim \rho_0(s)} \left[ B_M^\pi V_M(s_0) - B_M^\pi V_M(s_0) \right].

### A.1.2 Model-based formulation

Here we provide detailed derivation of the lower bound in Equation 9 in the main text.

**Assumption 1** Assume a scale $c$ and a function class $\mathcal{F}$ such that $V_M \in c\mathcal{F}$.

Following MOPO (Yu et al., 2020), we set $\mathcal{F} = \{ f : \|f\|_\infty \leq 1 \}$. In Section Preliminaries, we have that the reward function is bounded: $r(s, a) \in [-R_{max}, R_{max}]$. Thus, we have $\|V_M\|_\infty \leq \sum_{t=0}^{\infty} \gamma^t R_{max} = \frac{R_{max}}{1-\gamma}$.

As a direct corollary of Assumption 1 and Equation 5, we have

$$
\mathbb{E}_{s_0 \sim \rho_0(s)} \left[ B_M^\pi V_M(s_0) - B_M^\pi V_M(s_0) \right] \leq c \cdot \mathbb{E}_{s_0 \sim \rho_0(s)} \left[ d_{\mathcal{F}}(\hat{T}(s'|s, a), T(s'|s, a)) \right].
$$

Further, we find

$$
d_{\mathcal{F}}(\hat{T}(s'|s, a), T(s'|s, a)) \leq d_{\mathcal{F}}(\hat{T}(s'|s, a), \hat{T}(s'|s, a)) + d_{\mathcal{F}}(\hat{T}(s'|s, a), T(s'|s, a))
$$

For the first term $d_{\mathcal{F}}(\hat{T}(s'|s, a), \hat{T}(s'|s, a))$ in Equation 12, through Pinsker’s inequality, we have

$$
d_{\mathcal{F}}(\hat{T}(s'|s, a), \hat{T}(s'|s, a)) = D_{TV}(\hat{T}(s'|s, a), \hat{T}(s'|s, a)) \leq \sqrt{\frac{1}{2} D_{KL}(\hat{T}(s'|s, a), \hat{T}(s'|s, a))}
$$

To keep consistent with the DARA-based method-free offline methods, we introduce scale $\eta$ and bias $\delta$ to eliminate the square root in Equation 12. To be specific, we assume a scale $\eta$ and bias $\delta$ such that $\sqrt{\frac{1}{2} D_{KL}(\hat{T}, \hat{T})} \leq \eta D_{KL}(\hat{T}, \hat{T}) + \delta$. Thus, we obtain

$$
d_{\mathcal{F}}(\hat{T}(s'|s, a), \hat{T}(s'|s, a)) = D_{TV}(\hat{T}(s'|s, a), \hat{T}(s'|s, a)) \leq \eta D_{KL}(\hat{T}(s'|s, a), \hat{T}(s'|s, a)) + \delta
$$

In implementation, we clip the maximum deviation of $\log \frac{\hat{T}(s'|s, a)}{\hat{T}(s'|s, a)}$ for each $(s, a, s')$, which thus makes $D_{KL}(\hat{T}(s'|s, a), \hat{T}(s'|s, a))$ bounded.
For the second term $d_F(\hat{T}(s'|s, a), T(s'|s, a))$ in Equation 11 we assume that we have access to an oracle uncertainty qualification module that provides an upper bound on the error of the estimated empirical MDP $M := \{S, A, r, T, \rho_0, \gamma\}$.

**Assumption 2** Let $F$ be the function class in Assumption 4. We say $u : S \times A \rightarrow \mathbb{R}$ is an admissible error estimator for $\hat{T}$ if $d_F(\hat{T}(s'|s, a), T(s'|s, a)) \leq u(s, a)$ for all $(s, a)$.

Thus, we have

$$\mathbb{E}_{a, a' \sim d_{\text{argmax}}(\pi(a|s))} \left[ d_F(\hat{T}(s'|s, a), T(s'|s, a)) \right] \leq \mathbb{E}_{a, a' \sim d_{\text{argmax}}(\pi(a|s))} [u(s, a)]$$  \hspace{1cm} (14)

Bring Inequalities 10 and 11 into Lemma 3 we thus have

$$\eta_M(\pi) \geq \mathbb{E}_{s, a, s', s'' \sim d_F(\pi(a|s))} \left[ r(s, a) - \eta \gamma c \log \frac{\hat{T}'(s'|s, a)}{\hat{T}'(s'|s, a)} - \gamma cu(s, a) - \gamma \delta \right].$$  \hspace{1cm} (15)

### A.1.3 Learning Classifiers

Applying Bayes’ rule, we have

$$\hat{T}'(s'|a, s) := p(s'|s, a, \text{source}) = \frac{p(\text{source}|s, a, s')p(s, a, s')}{p(\text{source}|s, a)p(s, a)},$$

$$\hat{T}(s'|a, s) := p(s'|s, a, \text{target}) = \frac{p(\text{target}|s, a, s')p(s, a, s')}{p(\text{target}|s, a)p(s, a)}.$$  

Then we parameterize $p(\cdot|s, a, s')$ and $p(\cdot|s, a)$ with the two classifiers $q_{\text{source}}$ and $q_{\text{target}}$ respectively. Using the standard cross-entropy loss, we learn $q_{\text{source}}$ and $q_{\text{target}}$ with the following optimization objective:

$$\max \mathbb{E}_{(s, a, s') \sim D'} [\log q_{\text{source}}(\text{source}|s, a, s')] + \mathbb{E}_{(s, a, s') \sim D'} [\log q_{\text{target}}(\text{target}|s, a, s')],$$

$$\max \mathbb{E}_{(s, a) \sim D'} [\log q_{\text{source}}(s, a)] + \mathbb{E}_{(s, a) \sim D'} [\log q_{\text{target}}(s, a)].$$

With the trained $q_{\text{source}}$ and $q_{\text{target}}$, we have

$$\log \frac{\hat{T}'(s'|s, a)}{\hat{T}(s'|s, a)} = \log \frac{q_{\text{source}}(\text{source}|s, a, s')}{q_{\text{target}}(\text{source}|s, a)} - \log \frac{q_{\text{source}}(\text{target}|s, a, s')}{q_{\text{target}}(\text{target}|s, a)}.$$  \hspace{1cm} (16)

In our implementation, we also clip the above reward modification between $-10$ and $10$.

### A.2 Regularization View of Dynamics-Aware Reward Augmentation

Here we shortly characterize our dynamics-aware reward augmentation from the density regularization. Note the standard max-return objective $\eta_M(\pi)$ in RL can be written exclusively in terms of the on-policy distribution $d_{\text{argmax}}(\pi(a|s))$. To introduce an off-policy distribution $d_{\text{argmax}}(\pi(a|s))$ in the objective, prior works often incorporate a regularization (penalty): $D(d_{\text{argmax}}(\pi(a|s)))$, as in Equations 4 and 5. However, facing dynamics shift, such regularization should take into account the transition dynamics, which is penalizing $D(d_{\text{argmax}}(\pi(a|s)))d_{\text{argmax}}(\pi(a|s))T'(s'|s, a)$. From this view, it is also straightforward to derive the reward modification built on prior regularized off-policy max-return objective e.g., the off-policy approach AlgaeDICE (Nachum et al. 2019b).

In Table 4 we provide some related works with respect to the (state-action pair) $d_{\text{argmax}}(\pi(a|s))$ regularization and the (state-action-next-state pair) $d_{\text{argmax}}(\pi(a|s))T'(s'|s, a)$ regularization. We can find that the majority of the existing work focuses on regularizing state-action distribution, while dynamics shift receives relatively little attention. Thus, we hope to shift the focus of the community towards analyzing how the dynamics shift affects RL and how to eliminate the effect.
Table 4: Some related works with \textbf{explicit} (state-action $p(s, a)$ or state-action-next-state $p(s, a, s')$) \textbf{regularization}. More papers with respect to unsupervised RL, inverse RL (imitation learning), meta RL, multi-agent RL, and hierarchical RL are not included.

| Online: see summarization in Geist et al. (2019) and Vieillard et al. (2020). | reg. with $d_D(s)\pi_b(a|s)$ | Off-line (off-policy evaluation): | reg. with $d_{D'}(s)\pi_{b'}(a|s)\hat{T}'(s'|s, a)$ |
| --- | --- | --- | --- |
| (BCQ); | Eysenbach et al. (2021) (DARC) | Kumar et al. (2019) (BEAR); | Liu et al. (2021) (DARS); |
| (BRAC-p); | Abdolmaleki et al. (2018) (MPO); | Nair et al. (2020) (AWAC); | Haghgoo et al. (2021) |
| (AWR); | Siegel et al. (2020); | (CQL); | |
| (CRR); | Kumar et al. (2020) (CQL); | Kostrikov et al. (2021) (Fisher-BRC); | |
| (BAIL); | Nachum et al. (2019) (DualDICE); | Nachum et al. (2019) (AlgaeDICE); | |
| (CPQ); | Zhang et al. (2020) (GenDICE); | Yang et al. (2020); | |
| (MOPO); | Nachum & Dai (2020); | Jiang & Huang (2020); | |
| (COMBO); | Cang et al. (2021) (MABE); | Yu et al. (2020) (MOReL); | |

A.3 More Experiments

A.3.1 Training with $\{D' \cup D\}$

As we show in Figure 1 in Section Introduction, the performance of prior offline RL methods deteriorates dramatically as the amount of (target) offline data $D$ decreases. In Figure 4, we show that directly training with the mixed dataset $\{D' \cup D\}$ will not compensate for the deteriorated performance caused by the reduced target offline data, and training with such additional source offline data can even lead the performance degradation in some tasks.

Figure 4: Final performance on the D4RL (Walker2d) task: The orange bars denote the final performance with different amount (50% $D$, 20% $D$, 10% $D$, 5% $D$) of target offline data; The blue bars denote the final performance of mixing 100% of source offline data $D'$ and different amount of target data $x\%D$ ($x \in \{50, 20, 10, 5\}$, i.e., training with $\{100\%D' \cup x\%D\}$; The red lines denote the final performance of training with 100% of target offline data $D$. We can observe that 1) the performance deteriorates dramatically as the amount of (target) offline data decreases (100% $D$ (red line) $\rightarrow$ 50% $D$ (orange bar) $\rightarrow$ 20% $D$ (orange bar) $\rightarrow$ 10% $D$ (orange bar) $\rightarrow$ 5% $D$ (orange bar)), 2) after training with the additional 100% of source offline data, $\{100\%D' \cup x\%D\}$, the final performance is improved in some tasks, but most of the improvement is a pittance compared to the original performance degradation (compared to that training with the 100% of target offline data, i.e., the red lines), and 3) what is worse is that adding source offline data $D'$ even leads performance degradation in some tasks, e.g., CQL with 50% $D$ and 20% $D$ in Medium-Random.
A.3.2 COMPARISON BETWEEN LEARNING CLASSIFIERS AND LEARNING DYNAMICS (FOR THE REWARD MODIFICATION)

Table 5: Normalized scores for the Hopper tasks with the body mass (dynamics) shift. Rat. and Cla. denote estimating the reward modification with the estimated-dynamics ratio and learned classifiers (Appendix A.1.3), respectively.

| Body Mass Shift | BEAR | BRAC-p | AWR | BCQ | CQL | MOPO |
|-----------------|------|--------|-----|-----|-----|------|
| Hopper          | Rat. | Cla.   | Rat. | Cla. | Rat. | Cla. |
| Random          | 9.9  | > 8.4  | 11.2 | > 11.0 | 3.7  | < 4.5 |
| Medium          | 0.8  | < 1.6  | 31.7 | < 32.9 | 18.0 | < 28.9 |
| Medium-R        | 28.4 | < 34.1 | 36.5 | > 30.8 | 2.5  | < 4.2 |
| Medium-E        | 0.8  | < 1.2  | 50.9 | > 34.7 | 45.8 | < 26.6 |

In Table 5, we show the comparison between learning classifiers and learning dynamics (for our reward modification) in the Hopper tasks. We can observe that the two schemes for estimating the reward modification have similar performance. Thus, for simplicity and following Eysenbach et al. (2021), we adopt the classifiers to modify rewards in the source offline data in our experiments.

A.3.3 MORE EXAMPLES WITH RESPECT TO THE REWARD AUGMENTATION

Figure 5: We can observe that our reward augmentation 1) encourages ($-\Delta r > 0$, i.e., the green slice parts) these transitions ($-0.26 \leq \text{next-state[11]} \leq 0.26$) that have the same dynamics with the target environment, and 2) discourages ($-\Delta r < 0$, i.e., the red slice parts) these transitions that have different (unreachable) dynamics ($\text{next-state[11]} \leq -0.26$ or $\text{next-state[11]} \geq 0.26$) in the target.

In Figure 5, we provide more examples with respect to the reward augmentation in the Ant task in Figure 3 (left).

A.3.4 COMPARISON BETWEEN 10T, 1T, 1T+10S w/o Aug., AND 1T+10S DARA

Based on various offline RL algorithms (BEAR (Kumar et al., 2019), BRAC-p (Wu et al., 2019), BCQ (Fujimoto et al., 2019), CQL (Kumar et al., 2020a), AWR (Peng et al., 2019), MOPO (Yu et al., 2020), BC (behavior cloning), COMBO (Yu et al., 2021)), we provide the additional results in Tables 6, 7, 8, 9, and 10.

Table 6: Normalized scores for the Hopper tasks with the body mass (dynamics) shift. (The comparison results for BEAR, BRAC-p, AWR, CQL, and MOPO are provided in the main text.)

| Body Mass Shift | 10T 1T 1T+10S w/o Aug. 1T+10S DARA | 10T 1T 1T+10S w/o Aug. 1T+10S DARA |
|-----------------|-----------------------------------|-----------------------------------|
| Hopper          | BC COMBO                          | BC COMBO                          |
| Random          | 9.8 9.8 ↑ 6.9 ↑ 10.1 ↑            | 17.9 0.7 ↓ 5.4 ↑ 4.6 ↓            |
| Medium          | 29.0 27.9 ↓ 17.6 ↓ 25.0 ↑         | 94.9 1.8 ↓ 33.7 ↑ 45.7 ↑          |
| Medium-R        | 11.8 7.8 ↓ 7.7 ↓ 11.6 ↑           | 73.1 13.1 ↓ 11.0 ↑ 27.9 ↑         |
| Medium-E        | 111.9 21.5 ↓ 20.8 ↓ 35.7 ↑        | 1111.1 0.8 ↓ 14.9 ↑ 1081.1 ↑      |
Table 7: Normalized scores for the Hopper tasks with the joint noise (dynamics) shift.

| Joint Noise Shift | 10T | 1T | 1T+10S w/o Aug. | 1T+10S DARA | 10T | 1T | 1T+10S w/o Aug. | 1T+10S DARA | 10T | 1T | 1T+10S w/o Aug. | 1T+10S DARA |
|-------------------|-----|----|-----------------|--------------|-----|----|-----------------|--------------|-----|----|-----------------|--------------|
| **BEAR**          |     |    |                 |              |     |    |                 |              |     |    |                 |              |
| Random            | 11.4| 0.6| 7.4↑            | 4.2↑         | 11.0| 10.8↑| 10.0↑           | 10.8↑        | 10.2| 10.1↑          | 3.6↑         |
| Medium            | 52.1| 0.8| 2.0↑            | 2.0↑         | 32.7| 26.6↑| 27.6↑           | 37.6↑        | 35.9| 30.3↑          | 38.8↑        |
| Medium-R          | 33.7| 2.7| 3.6↑            | 9.9↑         | 0.6 | 13.4↑| 89.9↑           | 101.4↑       | 28.4| 12.4↑          | 6.7↑         |
| Medium-E          | 96.3| 0.8| 0.8↑            | 1.4↑         | 1.9 | 19.8↑| 57.6↑           | 87.8↑        | 27.1| 25.5↑          | 27.0↑        |
| **BRAC-p**        |     |    |                 |              |     |    |                 |              |     |    |                 |              |
| Random            | 10.6| 10.5| 7.0↑            | 9.6↑         | 10.8| 10.4↑| 10.4↑           | 10.8↑        | 11.7| 15.1↑          | 1.3↑         |
| Medium            | 54.5| 45.8| 49.0↑           | 54.4↑        | 58.0| 46.2↑| 58.0↑           | 58.0↑        | 28.0| 27.1↑          | 9.2↑         |
| Medium-R          | 33.1| 13.0| 23.8↑           | 32.0↑        | 48.6| 13.6↑| 2.6↑            | 3.6↑         | 67.5| 0.8↑           | 2.3↑         |
| Medium-E          | 110.9| 44.6| 96↑             | 109↑         | 98.7| 50.7↑| 73.4↑           | 108.9↑       | 23.7| 6.1↑           | 7.5↑         |
| **AWR**           |     |    |                 |              |     |    |                 |              |     |    |                 |              |
| Random            | 9.8 | 9.8↑| 7.5↑            | 9.1↑         | 17.9| 0.7↑| 1.8↑            | 4.9↑         |      |              |              |
| Medium            | 11.8| 7.8↑| 8.5↑            | 11.3↑        | 73.1| 13.1↑| 4.0↑            | 9.6↑         |      |              |              |
| Medium-E          | 111.9| 21.5| 53.5↑           | 77.9↑        | 111.1| 0.8↑| 34.0↑           | 45.9↑        |      |              |              |

Table 8: Normalized scores for the Walker2d tasks with the body mass (dynamics) shift. (The comparison results for BEAR, BRAC-p, AWR, CQL, and MOPO are provided in the main text.)

| Body Mass Shift | 10T | 1T | 1T+10S w/o Aug. | 1T+10S DARA | 10T | 1T | 1T+10S w/o Aug. | 1T+10S DARA | 10T | 1T | 1T+10S w/o Aug. | 1T+10S DARA |
|-----------------|-----|----|-----------------|--------------|-----|----|-----------------|--------------|-----|----|-----------------|--------------|
| **BC**          |     |    |                 |              |     |    |                 |              |     |    |                 |              |
| Random          | 1.6 | 0.1 | 1.7↑            | 2.7↑         | 7.0 | 1.8↑| 2.0↑            | 3.5↑         |      |              |              |
| Medium          | 6.6 | 5.5 | 3.8↑            | 6.6↑         | 75.5| -1.0↑| 23.9↑           | 36.6↑        |      |              |              |
| Medium-R        | 11.3| 6.6 | 8.1↑            | 11.0↑        | 56.0| 0.1↑| 11.4↑           | 22.6↑        |      |              |              |
| Medium-E        | 6.4 | 3.1 | 6.0↑            | 6.2↑         | 96.1| -0.9↑| -0.1↑           | -0.1↑        |      |              |              |
| **COMBO**       |     |    |                 |              |     |    |                 |              |     |    |                 |              |
| Random          | 9.9 | 9.8↑| 7.5↑            | 9.1↑         | 17.9| 0.7↑| 1.8↑            | 4.9↑         |      |              |              |
| Medium          | 11.8| 7.8↑| 8.5↑            | 11.3↑        | 73.1| 13.1↑| 4.0↑            | 9.6↑         |      |              |              |
| Medium-E        | 111.9| 21.5| 53.5↑           | 77.9↑        | 111.1| 0.8↑| 34.0↑           | 45.9↑        |      |              |              |

Table 9: Normalized scores for the Walker2d tasks with the joint noise (dynamics) shift.

| Joint Noise Shift | 10T | 1T | 1T+10S w/o Aug. | 1T+10S DARA | 10T | 1T | 1T+10S w/o Aug. | 1T+10S DARA | 10T | 1T | 1T+10S w/o Aug. | 1T+10S DARA |
|-------------------|-----|----|-----------------|--------------|-----|----|-----------------|--------------|-----|----|-----------------|--------------|
| **BEAR**          |     |    |                 |              |     |    |                 |              |     |    |                 |              |
| Random            | 7.3 | 2.2 | 0.6↓            | 2.6↑         | -0.2| 2.8↑| 3.3↑            | 8.8↑         | 1.5 | 0.9↑| 1.5↑            | 1.5↑         |
| Medium            | 59.1| -0.4| 0.6↑            | 0.1↑         | 77.5| 28.8↑| 55.2↑           | 72.9↑        | 17.4| 12.2↑| 17.2↑           | 17.2↑        |
| Medium-R          | 19.2| 0.4 | 4↑              | 10.4↑        | -0.3| 6.3↑| 32.1↑           | 34.8↑        | 15.5| 6↑             | 1.4↑         |
| Medium-E          | 40.1| -0.2| 0.8↑            | 0.6↑         | 76.9| 21.8↑| 62.3↑           | 74.3↑        | 53.8| 40.4↑| 53↑             | 53.6↑        |
| **BRAC-p**        |     |    |                 |              |     |    |                 |              |     |    |                 |              |
| Random            | 4.9 | 3.7 | 3.4↑            | 5.2↑         | 7.0 | 5.5↑| 2.7↑            | 6.4↑         | 13.6| -0.3↑| -0.2↑           | -0.2↑        |
| Medium            | 53.1| -43 | 44.9↑           | 52.7↑        | 79.2| 43.9↑| 73.2↑           | 81.2↑        | 17.8| 5.8↑| 7.8↑            | 12.2↑        |
| Medium-R          | 15  | 5.7 | 9.8↑            | 14.6↑        | 26.7| 1.8↑| 1.4↑            | 1.8↑         | 39  | 0.8↑| 9.3↑            | 16.4↑        |
| Medium-E          | 57.5| 44.5| 40.6↑           | 57.2↑        | 111 | 46.8↑| 109.9↑          | 116.5↑       | 44.6| 2.9↑| 15.2↑           | 26.3↑        |
| **AWR**           |     |    |                 |              |     |    |                 |              |     |    |                 |              |
| Random            | 1.6 | 0.1 | 0.9↑            | 1.6↑         | 7.0 | 1.8↑| 0.1↓            | 1.5↑         |      |              |              |
| Medium            | 6.6 | 5.5 | 6.4↑            | 6.5↑         | 75.5| -1.0↑| 0.4↑            | 0.7↑         |      |              |              |
| Medium-R          | 11.3| 6.6 | 4.6↑            | 10.4↑        | 56.0| 0.1↑| 5.6↑            | 7.4↑         |      |              |              |
| Medium-E          | 6.4 | 3.1 | 6.2↑            | 6.4↑         | 96.1| -0.9↑| 0.8↑            | -0.1↓        |      |              |              |
Table 10: Normalized scores for the Halfcheetah tasks with the joint noise (dynamics) shift.

| Joint Noise Shift | 10T | IT | 1T+10S w/o Aug. | 1T+10S BRAC-p | 1T+10S DARA | BEAR | BRAC-p | AWR |
|-------------------|-----|----|-----------------|---------------|-------------|------|--------|-----|
| Halfcheetah        |     |    |                 |               |             |      |        |     |
| Random            | 25.1| 17.8| 25.0↑           | 25.1↑         | 24.1↑       | 21.0↓| 25.0↑  | 26.7↑|
| Medium            | 41.7| -0.2| 0.8↑            | 1.5↑          | 43.8↑       | 43.0↑| 52.4↑  | 53.0↑|
| Medium-R          | 38.6| 9.3 | -0.6↑           | -0.5↑         | 45.4↑       | 2.5↑ | -23.3↑ | 45.3↑|
| Medium-E          | 53.4| -1.2| 1.0↑            | -1.4↑         | 44.2↑       | 6.9↑ | 0.9↑   | 45.3↑|
| Medium-E          | 64.7| 37.3| 55.3↑           | 76.9↑         | 62.4↑       | 3.3↑ | 7.7↑   | 1.7↑ |
| BC                |     |    |                 |               |             |      |        |     |
| Random            | 2.2 | 2.3 | 2.2↑            | 2.3↑          | 35.4↑       | -2.3↓| -2.4↑  | 10.4↑|
| Medium            | 40.7| 37.6| 40.0↑           | 48.6↑         | 44.4↑       | 35.4↑| 40.7↑  | 52.6↑|
| Medium-R          | 38.2| 1.1 | 39.4↑           | 41.3↑         | 46.2↑       | 0.6↑ | 2.0↑   | 1.9↑ |
| Medium-E          | 35.8| 36.3| 49.0↑           | 49.3↑         | 90.0↑       | 4.4↑ | 6.5↑   | 11.1↑|
| MABE              |     |    |                 |               |             |      |        |     |
| Random            |     |    |                 |               |             |      |        |     |
| Medium            |     |    |                 |               |             |      |        |     |

Table 11: Normalized scores in the (target) D4RL Hopper tasks with the joint noise shift., where "Tune" denotes baseline “fine-tune”.

| Joint Noise Shift | Tune | DARA | BEAR | BRAC-p | BCQ | CQL | MOPO | MABE |
|-------------------|------|------|------|--------|-----|-----|------|------|
| Random            | 0.8  | 4.2↑ | 6.4↑ | 10.8↑  |     |     |      |      |
| Medium            | 1.9  | 2.0↑ | 44.9↑| 37.6↑  |     |     |      |      |
| Medium-R          | 0.7  | 9.9↑ | 32.4↑| 101.4↑ |     |     |      |      |
| Medium-E          | 0.8  | 1.4↑ | 98.2↑| 87.8↑  |     |     |      |      |
| Medium-E          | 0.7  | 9.9↑ | 32.4↑| 101.4↑ |     |     |      |      |

Table 12: Normalized scores in the (target) D4RL Walker2d tasks with the joint noise shift., where "Tune" denotes baseline “fine-tune”.

| Joint Noise Shift | Tune | DARA | BEAR | BRAC-p | BCQ | CQL | MOPO | MABE |
|-------------------|------|------|------|--------|-----|-----|------|------|
| Random            | 2.7  | 2.6↓ | 1.4↑ | 8.8↑   |     |     |      |      |
| Medium            | 0.5  | 1.1↑ | 55.8↑| 72.9↑  |     |     |      |      |
| Medium-R          | 3.2  | 10.4↑| 12.2↓| 23.4↑  |     |     |      |      |
| Medium-E          | -0.4 | 0.6↑ | 71.7↑| 74.3↑  |     |     |      |      |

A.3.5 Comparison with the cross-domain based baselines

In Tables [11] and [12] we provide the comparison between our DARA-based methods, fine-tune based methods, and MABE-based methods in Hopper and Walker2d tasks, over the dynamics shift concerning the joint noise of motion. We can observe that in a majority of tasks, our DARA-based methods outperforms the fine-tune-based method (67%↑ vs. 13%↓, including the results in the main text). Moreover, our DARA can achieve comparable or better performance compared to MABE-based baselines on eleven out of sixteen tasks (including the results in the main text).

A.3.6 Additional results on the quadruped robot

In this offline sim2real setting, we collect the source offline data in the simulator (10⁶ or 2 * 10⁶ steps) and target offline data in the real world (3 * 10⁵ steps). See Appendix [A.4] for details. For testing, we directly deploy the learned policy in the real (flat or obstructive) environment and adopt the average distance covered in an episode (300 steps) as our evaluation metrics.
We first deploy our learned policy in the flat and static environment. The results (distance covered in an episode) are provided in Table 13. We find that with Medium-R offline data, w/o Aug. BCQ and DARA BCQ both could not acquire the locomotion skills, which we think is caused by the lack of high-quality offline data. With more “expert” data (Medium-R → Medium → Medium-E, or Medium-R → Medium-R-E), w/o-Aug. BCQ allows for progressive performance (0.00 → 1.56 → 2.16, or 0.00 → 1.69 in BCQ), but with our reward augmentation, such performance can be further improved (with average improvement 13.6%).

2) CQL (Figure 8): We find that with Medium-R or Medium-R-E offline data, w/o Aug. CQL and DARA CQL both could not learn the locomotion skills, which we think is caused by the low-quality “Replay” offline data. With Medium or Medium-E offline data, w/o Aug. CQL and DARA CQL acquire similar performance on this flat and static environment.

3) MOPO: We find that the model-based MOPO (both w/o Aug. and DARA) could hardly learn the locomotion skill under the provided offline data.

We then deploy our learned policy in the obstructive and dynamic environment. The results (distance covered in an episode) are provided in Table 14. We find that with more “expert” data (Medium → Medium-E → Medium-R-E), w/o Aug. BCQ allows for progressive performance (0.85 → 1.15 → 1.27), and with our reward augmentation, such performance can be further improved (with average improvement 25.9%). At the same time, we can also find that due to the presence of environmental obstacles, the performance of both w/o...
Aug. BCQ and w/o Aug. DARA is decreased compared to the deployment on the flat environment. However, we find that our DARA exhibits greater average performance improvement under this obstructive environment (13.6% → 25.9%) compared to that in the flat environment. These results demonstrate that our DARA can learn an adaptive policy for the target environment and thus show a greater advantage over w/o-Aug. in more complex environments.

2) CQL (Figure 10): Similar to BCQ, our DARA CQL exhibits a greater performance improvement over baseline in the obstructive and dynamic environment (0.2% → 30.9%) compared to that in the flat and static environment.

In summary, The results in the quadruped robot tasks support our conclusion in the main text regarding the dynamics shift problem in offline RL — with only modest amounts of target offline data (3 * 10^4 steps), DARA-based methods can acquire an adaptive policy for the (both flat and obstructive) target environment and exhibit better performance compared to baselines under the dynamics adaptation setting.

Figure 7: Deployment on the flat and static environment of BCQ.

Figure 8: Deployment on the flat and static environment of CQL.
A.3.7 ABSTRACTION STUDY WITH RESPECT TO THE AMOUNT OF TARGET OFFLINE DATA

To see whether the amount of target offline data can be further reduced, we show the results of the ablation study with respect to the amount of target offline data in Tables 15 and 16.

Table 15: Ablation study with respect to the amount of target Hopper data (body mass shift tasks). 10%, 5% and 1% denote training with 10%, 5% and 1% of target offline data, respectively, and additional 100% source offline data.

| Body Mass Shift | 10% | 5% | 1% | 10% | 5% | 1% | 10% | 5% | 1% | 10% | 5% | 1% |
|-----------------|-----|----|----|-----|----|----|-----|----|----|-----|----|----|
| **Hopper**      |     |    |    |     |    |    |     |    |    |     |    |    |
| Medium-R        | 34.1| 10.7| 6.4| 30.8| 27.7| 20.0| 32.8| 20.5| 16.3| 3.7 | 3.2 | 2.3|
| Medium-E        | 1.2 | 0.6 | 0.6| 34.7| 25.1| 20.6| 84.2| 65.1| 55.6| 99.7| 52.3| 38.5|

Table 16: Ablation study with respect to the amount of target Walker2d data (body mass shift tasks). 10%, 5% and 1% denote training with 10%, 5% and 1% of target offline data, respectively, and additional 100% source offline data.

| Body Mass Shift | 10% | 5% | 1% | 10% | 5% | 1% | 10% | 5% | 1% | 10% | 5% | 1% |
|-----------------|-----|----|----|-----|----|----|-----|----|----|-----|----|----|
| **Walker2d**    |     |    |    |     |    |    |     |    |    |     |    |    |
| Medium-R        | 7.3 | 5.9 | 1.3| 18.6| 21.6| 15.8| 15.1| 12.7| 9.7 | 2.0 | 1.3 | 0.5|
| Medium-E        | 2.3 | -0.2| -0.3| 77.5| 2.0 | -0.2| 57.2| 29.7| 20.6| 93.3| 0.1 | -0.3|

A.3.8 ILLUSTRATION OF WHETHER THE LEARNED POLICY IS LIMITED TO THE SOURCE OFFLINE DATA

If we directly perform DARA with only the source offline data $D'$, the learned behaviors will be restricted to the source offline data. For example, in the Map task, collecting source dataset with the obstacle and collecting target dataset without the obstacle. In this case, it can be harder for DARA (with only the source $D'$) to capture the change in the transition dynamics, thus harder for the agent...
to figure out the new optimal policy (the shorter path without the obstacle). However, as stated in Algorithm 1, we perform offline RL algorithms with both target offline data and source offline data \( \{D' \cup D\} \). Thus, to some extent, such limitation can be overcome as long as offline RL algorithm captures the information (e.g. the short path without the obstacle) contained in the (limited) target \( D \), see Figure 11 for the illustration.

Figure 11: We exchange the source environment and the target environment in Figure 2 (in the main text) so that the source environment has an obstacle and the target environment has no obstacles. In the source domain, we collect 100k of random transitions. In the target domain, we collect 0k, 1k, 2k, 5k, and 10k random transitions respectively. We set \( \eta = 0.1 \). We can find that if we perform DARA with only source offline data \( D' \) (i.e., 0k target data), we indeed can not acquire the optimal trajectory (e.g. the short path without the obstacle). However, even there is no transition of passing through obstacles in the source data, performing DARA with \( \{D' \cup D\} \) enables us to acquire the behavior of moving through obstacles. As we increase the number of target offline data \( D \), training with \( \{D' \cup D\} \) can gradually acquire optimal trajectories.

A.3.9 COMPARISON BETWEEN DARA AND IMPORTANCE SAMPLING (IS) BASED DYNAMICS CORRECTION

In Table 17, we report the experimental comparison between DARA and importance sampling based dynamics adaption. We can find that in most of the tasks, our DARA performs better than the IS-based approaches.

| Body Mass Shift | IS | DARA | IS | DARA | IS | DARA |
|----------------|----|------|----|------|----|------|
| **Hopper**    |    |      |    |      |    |      |
| Random        | 4.6 ± 2.8 | 8.4 ± 1.2 | 10.8 ± 0.5 | 11 ± 0.6 | **10.2 ± 0.3** | 4.5 ± 0.9 |
| Medium        | 1 ± 0.4 | **1.6 ± 1** | 17.4 ± 10.6 | **32.9 ± 7.5** | 24.8 ± 7.7 | **28.9 ± 5.5** |
| Medium-R      | 17.3 ± 4.7 | **34.1 ± 5.8** | 21.6 ± 8.3 | **30.8 ± 4.9** | **14 ± 2.2** | 4.2 ± 3.5 |
| Medium-E      | 0.8 ± 0.2 | **1.2 ± 0.5** | **36 ± 13.5** | 34.7 ± 8.5 | **29.3 ± 2.6** | 26.6 ± 2 |
| **Hopper**    |    |      |    |      |    |      |
| Random        | 9.2 ± 1.1 | **9.7 ± 0.2** | 10.3 ± 0.4 | **10.4 ± 0.4** | **2.8 ± 3** | 2.1 ± 1.7 |
| Medium        | 28.2 ± 8.8 | **38.4 ± 1.8** | 43.3 ± 10 | **59.3 ± 12.2** | 7.6 ± 7.2 | **10.7 ± 5.1** |
| Medium-R      | 14.2 ± 1.3 | **32.8 ± 0.9** | 2.2 ± 0.3 | **3.7 ± 1.4** | 4.9 ± 3.8 | **8.4 ± 3.5** |
| Medium-E      | 83.4 ± 23.7 | **84.2 ± 9.8** | 87.8 ± 16.9 | **99.7 ± 16.4** | 4.6 ± 2.9 | **5.8 ± 2.3** |

A.3.10 THE SENSITIVITY OF THE COEFFICIENT OF THE REWARD MODIFICATION

In Table 18, we check the sensitivity of hyper-parameter \( \eta \), i.e., the coefficient of the reward modification in \( r(s, a) - \eta \Delta r(s, a, s') \).
Table 18: We show the normalized scores for the Hopper tasks with body mass shift, by varying $\eta \in \{0, 0.05, 0.1, 0.2, 0.5\}$ over BEAR, BRAC-p, AWR, BCQ, CQL, and MOPO.

| Body Mass Shift | Hyper-parameter $\eta$ | 0   | 0.05 | 0.1  | 0.2  | 0.5  |
|-----------------|------------------------|-----|------|------|------|------|
|                 | BEAR                   |     |      |      |      |      |
| Hopper          | Random                 | 4.6 | 7.7  | 8.4  | 7    | 4.2  |
|                 | Medium                 | 0.9 | 1.1  | 1.6  | 0.9  | 0.7  |
|                 | Medium-R               | 18.2| 28.5 | 34.1 | 29.1 | 18.1 |
|                 | Medium-E               | 0.6 | 0.8  | 1.2  | 1.2  | 0.7  |
|                 | BRAC-p                 |     |      |      |      |      |
| Hopper          | Random                 | 9.6 | 11.2 | 11   | 10.6 | 5.3  |
|                 | Medium                 | 29.2| 31.8 | 32.9 | 26.6 | 16.7 |
|                 | Medium-R               | 20.1| 17.8 | 30.8 | 13.9 | 10.4 |
|                 | Medium-E               | 32.3| 40.4 | 34.7 | 29.4 | 25.2 |
|                 | AWR                    |     |      |      |      |      |
| Hopper          | Random                 | 3.4 | 4.1  | 4.5  | 3.4  | 2.5  |
|                 | Medium                 | 20.8| 26.5 | 28.9 | 26.6 | 17.4 |
|                 | Medium-R               | 4.1 | 3   | 4.2  | 2.6  | 4.3  |
|                 | Medium-E               | 26.8| 27  | 26.6 | 17.8 | 24.2 |
|                 | BCQ                    |     |      |      |      |      |
| Hopper          | Random                 | 8.3 | 9.6  | 9.7  | 7.4  | 7.6  |
|                 | Medium                 | 25.7| 26.5 | 38.4 | 27.1 | 26.7 |
|                 | Medium-R               | 28.7| 29.5 | 32.8 | 25.9 | 21.2 |
|                 | Medium-E               | 75.4| 70.4 | 84.2 | 67.9 | 61.9 |
|                 | CQL                    |     |      |      |      |      |
| Hopper          | Random                 | 10.2| 10   | 10.4 | 10   | 10   |
|                 | Medium                 | 44.9| 59.8 | 59.3 | 44.2 | 37.1 |
|                 | Medium-R               | 1.4 | 2.1  | 3.7  | 3.9  | 3.4  |
|                 | Medium-E               | 53.6| 65.3 | 99.7 | 60.5 | 75.9 |
|                 | MOPO                   |     |      |      |      |      |
| Hopper          | Random                 | 2   | 1.8  | 2.1  | 1.2  | 0.8  |
|                 | Medium                 | 5   | 6.5  | 10.7 | 5.3  | 2.8  |
|                 | Medium-R               | 5.5 | 7.5  | 8.4  | 5.7  | 1.9  |
|                 | Medium-E               | 4.8 | 8.1  | 5.8  | 4.7  | 2.1  |
A.4 Environments and Dataset

![Image of tasks considered in this work]

Figure 12: Illustration of the suite of tasks considered in this work: (from left to right) Hopper, Walker2d, HalfCheetah, simulated and real-world quadruped robots. These tasks require the RL agent to learn locomotion gaits for the illustrated characters.

In this work, the tasks include Hopper, Walker2d, HalfCheetah, simulated (see the dynamics parameters in Zhang et al.) and real-world quadruped robot, which are illustrated in Figure [12].

Table 19: Dynamics shift for Hopper, Walker2d, and HalfCheetah tasks. For the body mass shift, we change the mass of the body in the source MDP \( M' \). For the joint noise shift, we add a noise (randomly sampling in \([-0.05, +0.05]\)) to the actions when we collect the source offline data, i.e., \( D' := \{(s, a, r, s')\} \sim d_{M'}(s) \pi_{b'}(a|s) r(s, a) T'(s'|s, a + \text{noise}) \).

| Task   | Body Mass Shift | Joint Noise Shift |
|--------|-----------------|-------------------|
| Hopper | mass[1]=2.5     | action[1]+noise   |
| Walker2d | mass[1]=1.47    | action[1]+noise   |
| HalfCheetah | mass[4]=0.5   | action[1]+noise   |

In the Hopper, Walker2d and HalfCheetah dynamics adaptation setting, we set the D4RL (Fu et al., 2020) dataset as our target domain. For the source dynamics, we change the body mass (body mass shift) or add noises to joints (joint noise shift) of the agents (see Table [19] for the details) and then collect the source offline dataset in the changed environment. Following Fu et al. (2020), on the changed source environment, we collect the 1) "Random" offline data, generated by unrolling a randomly initialized policy, 2) "Medium" offline data, generated by a trained policy with the "medium" level of performance in the source environment, 3) "Medium-Replay" (Medium-R) offline data, consisting of recording all samples in the replay buffer observed during training until the policy reaches the "medium" level of performance, 4) "Medium-Expert" (Medium-E) offline data, mixing equal amounts of expert demonstrations and "medium" data in the source environment.

In the sim2real setting (for the quadruped robot), we use the A1 dog from Unitree (Wang, 2020). We collect the target offline data using five target behavior policies in the real-world with changing terrains, as shown in Figure [13] and collect the "Medium", "Medium-Replay" (Medium-R), "Medium-Expert" (Medium-E), "Medium-Replay-Expert" (Medium-R-E) source offline data in the simulator, where "Medium-Replay-Expert" denotes mixing equal amounts of "Medium-Replay" data and expert demonstrations in the simulator. In Section [A.5] we provide the details of how to obtain the target and source behavior policy, so as to collect our target and source offline data.

We list our tasks properties in Table [20] and provide our collected dataset in supplementary material. In implementation, we set \( \eta = 0.1 \) for all simulated tasks and set \( \eta = 0.01 \) for the sim2real task. In Table [18] we also report the sensitivity of DARA on the hyper-parameters \( \eta \).

A.5 Training the (Target and Source) Behavior Policy for the Quadruped Robot

To obtain a behavior policy that can be deployed in simulator (for collecting the source offline data) or real-world (for collecting the target offline data), we introduce the prior knowledge (Iscen et al., 2018) and domain randomization (Tobin et al., 2017; Peng et al., 2018).
which represents swing phase if

\[ \phi \]

the robot locomotion, we designed a compound cycloid trajectory (Sakakibara et al., 1990) as prior

\[ \theta = \begin{bmatrix} 0 & 0 & 0 \end{bmatrix} + \begin{bmatrix} x \ y \ z \end{bmatrix} \]

At every time step \( t \), \( \phi_i = (t \cdot f_0 + \phi_0[i] + \phi_{\text{offset}}[i]) \mod 2T_m \) where \( T_m = 0.3 \), and \( f_0 = 1.1 \) is the base frequency, and \( \phi_0 = [0, 0.3, 0.3, 0] \) is the initial phase. \( \phi_{\text{offset}} \) is part of the output of the controller. The trajectory of the swing leg is:

\[
\begin{align*}
  x_i &= S \left[ \frac{t}{T_m} - \frac{1}{2\pi} \sin \left( \frac{2\pi t}{T_m} \right) \right] + S_0, \quad i = 1, 2 \\
  y_i &= Y_0 \\
  z_i &= H \left[ \text{sgn} \left( \frac{T_m}{2} - t \right) \left( 2f_E(t) - 1 \right) + 1 \right] + Z_0
\end{align*}
\]

where

\[
f_E(t) = \frac{t}{T_m} - \frac{1}{4\pi} \sin \left( \frac{4\pi t}{T_m} \right),
\]

and

\[
\text{sgn} \left( \frac{T_m}{2} - t \right) = \begin{cases} 
  1 & 0 \leq t < \frac{T_m}{2} \\
  -1 & \frac{T_m}{2} \leq t < T_m
\end{cases}
\]
The trajectory of the standing leg is:

\[
\begin{align*}
x_i &= S \left( \frac{2T_m-t}{T_m} + \frac{1}{2} \sin \left( \frac{2\pi t}{T_m} \right) \right) + S_0, \quad i = 1, 2 \\
x_i &= S \left( \frac{2T_m-t}{T_m} + \frac{1}{2} \sin \left( \frac{2\pi t}{T_m} \right) \right) - S + S_0, \quad i = 3, 4 \\
y &= Y_0 \\
z &= Z_0
\end{align*}
\]

where \( S = 0.14m, H = 0.18m \) are the maximum foot length and height. \( S_0 = [0.17, 0.17, -0.2, -0.2], Y_0 = [-0.13, 0.13, -0.13, 0.13], Z_0 = [-0.32, -0.32, -0.32, -0.32] \) are the default target foot position in body frame.

**Domain Randomization:** To encourage the policy to be robust to variations in the dynamics, we incorporate the domain randomization. In Table 21 we provide the dynamics parameters and their respective range of values.

| Parameter            | Range                        |
|----------------------|------------------------------|
| Mass                 | \([0.95, 1.1]\) \times \text{default value} |
| Inertia              | \([0.80, 1.2]\) \times \text{default value} |
| Motor Strength       | \([0.80, 1.2]\) \times \text{default value} |
| Latency              | \([0, 0.04]\) s              |
| Lateral Friction     | \([0.5, 1.25]\) Ns/m         |
| Joint Friction       | \([0, 0.05]\) Nm             |

**State Space, Action Space and Reward Function:** The action is a 16-dimensional vector consisting of leg phase and target foot position residuals in the body frame. The design of state space and reward function mainly follows the prior work Lee et al. (2020). In Table 22 we provide the state representation.

| Data                     | Dimension |
|--------------------------|-----------|
| Desired direction        | 2         |
| Euler angle (\( rpy \))  | 3         |
| Base angular velocity    | 3         |
| Base linear velocity     | 3         |
| Joint position/velocity  | 24        |
| FTG phases (\( \phi_i \)) | 8         |
| FTG frequencies (\( f_i \)) | 4         |
| Base frequency (\( f_o \)) | 1         |
| Joint position error history | 24        |
| Joint velocity history   | 24        |
| Foot target history      | 24        |

The reward function is defined as

\[
0.1r_{lv} + 0.05r_y + 0.05r_{rp} + 0.005r_b + 0.02r_{be} + 0.025r_s + 2 \cdot 10^{-5}r_\tau.
\]

The individual terms are defined as follows.

1) Linear velocity reward \( r_{lv} \):

\[
r_{lv} := \begin{cases} 
\exp(-30|v_{pr} - 0.2|) & v_{pr} < 0.2 \\
1 & v_{pr} \geq 0.2 
\end{cases}
\]
where $v_{pr} = v_{xy} \cdot \hat{v}_{xy}$ is the base linear velocity projected onto the command direction.

2) Yaw angle reward $r_y$:

$$r_y := \exp(-(y - \hat{y})^2),$$

where $y$ and $\hat{y}$ is the yaw and desired yaw angle.

3) Roll and pitch reward $r_{rp}$:

$$r_{rp} := \exp(-1.5 \sum (\phi - [0, \arccos(\frac{<P_{xz}, (0, 0, 1)^T>}{\|P_{xz}\|}) - \pi/2])^2),$$

where $\phi$ are the roll and pitch angle. $P_{xz} = P_1 - P_4$ or $P_{xz} = P_2 - P_3, P_i \in [1, 4]$ are the foot position in world frame. The advantage of designing the target pitch angle in this way is to ensure that the body of the robot is parallel to the supporting surface of the stand legs, thereby ensuring that the robot can smoothly over challenge terrain, such as upward stairs.

4) Base motion reward $r_b$:

$$r_b := \exp(-1.5 \sum (v_{xy} - v_{pr} \ast \hat{v}_{xy})^2) + \exp(-1.5 \sum (\omega_{xy})^2),$$

where $\omega_{xy}$ are the roll and pitch rates.

5) Body collision reward $r_{bc}$:

$$r_{bc} := -|I_{body}/I_{foot}|,$$

where $I_{body}$ and $I_{foot}$ are the contact numbers of robot’s body parts and foot with the terrain, respectively.

6) Target smooth reward $r_s$:

$$r_s := -\|f_{d,t} - 2f_{d,t-1} + f_{d,t-2}\|,$$

where $f_{d,i}(i = t, t-1, t-2)$ are the target foot positions in the time-step $t$, $t-1$ and $t-2$.

7) Torque reward $r_{\tau}$:

$$r_{\tau} := -\sum |\tau_i|,$$

where $\tau_i$ is the joint torques.

**Training Details:** Both the behavior policy and value networks are Multilayer Perceptron (MLP) with 3 hidden layers, which have 256, 128 and 64 nodes. The activation function is the $\text{Tanh}$ function, and the optimizer is $\text{Adam}$. With the above prior knowledge, domain randomization and reward function, we train our behavior policy with SAC (Haarnoja et al., 2018) in PyBullet (Coumans & Bai, 2016–2021).

### A.6 Additional Results

Here we provide additional results regarding the error bars (Tables 23 and 24).
Table 23: Normalized scores for the D4RL tasks (with body mass shift). We take the baseline results (for 10T) of MOPO from their original papers and that of the other model-free methods (BEAR, BRAC-p, AWR, BCQ and CQL) from the D4RL paper [Fu et al., 2020].

| Body Mass Shift | 10T  | 1T  | 1T+10S w/o Aug. | 1T+10S (DARA) | 10T  | 1T  | 1T+10S w/o Aug. | 1T+10S (DARA) | 10T  | 1T  | 1T+10S w/o Aug. | 1T+10S (DARA) |
|----------------|------|-----|-----------------|----------------|------|-----|-----------------|----------------|------|-----|-----------------|----------------|
|                | BEAR |     |                 |                 | AWR  |     |                 |                 |      |     |                 |                 |
| Hopper         |      |     |                 |                 |      |     |                 |                 |      |     |                 |                 |
| Random         | 11.4 | 1 ± 0.5 | 4.6 ± 3.4 | 8.4 ± 1.2 | 11   | 10.9 ± 0.1 | 9.6 ± 3.3 | 11 ± 0.6 | 10.2 | 10.3 ± 0.3 | 3.4 ± 0.7 | 4.5 ± 0.9 |
| Medium         | 52.1 | 0.8 ± 0 | 0.9 ± 0.3 | 1.6 ± 1   | 32.7 | 29 ± 62   | 29.2 ± 2.1 | 32.9 ± 7.5 | 35.9 | 30.9 ± 0.4 | 20.8 ± 6.3 | 28.9 ± 5.5 |
| Medium-R       | 33.7 | 1.3 ± 1.5 | 18.2 ± 5  | 34.1 ± 5.8 | 0.6  | 5.4 ± 3.3 | 20.1 ± 4.8 | 30.8 ± 4.9 | 28.4 | 8.8 ± 4.9  | 4.1 ± 1.7  | 4.2 ± 3.5  |
| Medium-E       | 96.3 | 0.8 ± 0.1 | 0.6 ± 0   | 1.2 ± 0.5 | 1.9  | 34.5 ± 14.7| 32.3 ± 7.8 | 34.7 ± 8.5 | 27.1 | 27 ± 1.3   | 26.8 ± 0.4 | 26.6 ± 2   |
|                |      |     |                 |                 |      |     |                 |                 |      |     |                 |                 |
| Random         | 10.6 | 10.6 ± 0.1 | 8.3 ± 0.3 | 9.7 ± 0.2 | 10.8 | 10.6 ± 0.1 | 10.2 ± 0.3 | 10.4 ± 0.4 | 11.7 | 4.8 ± 2.4  | 2 ± 2.1    | 2.1 ± 1.7  |
| Medium         | 54.5 | 37.1 ± 6.3 | 25.7 ± 5.5 | 38.4 ± 1.8 | 58   | 43 ± 9.2  | 44.9 ± 2.7 | 59.3 ± 12.2 | 28   | 4.1 ± 2    | 5 ± 5.3    | 10.7 ± 5.1 |
| Medium-R       | 33.1 | 9.3 ± 4.4 | 28.7 ± 1.9 | 32.8 ± 0.9 | 48.6 | 9.6 ± 5.2 | 1.4 ± 0.3 | 3.7 ± 1.4 | 67.5 | 1 ± 0.6    | 5.5 ± 4.6  | 8.4 ± 3.5  |
| Medium-E       | 110.9 | 58 ± 16.2 | 75.4 ± 7.8 | 84.2 ± 9.8 | 98.7 | 59.7 ± 34.5 | 53.6 ± 21.2 | 99.7 ± 16.4 | 23.7 | 1.6 ± 0.6  | 4.8 ± 2.9  | 5.8 ± 2.3  |
|                |      |     |                 |                 |      |     |                 |                 |      |     |                 |                 |
| Random         | 7.3  | 1.5 ± 0.9 | 3.1 ± 0.9 | 3.2 ± 0.4 | -0.2 | 0 ± 0.2 | 1.3 ± 0.7 | 3.2 ± 2.5 | 1.5  | 1.3 ± 0.4  | 2 ± 1      | 2.4 ± 0.8  |
| Medium         | 59.1 | -0.5 ± 0.3 | 0.6 ± 0.5 | 0.3 ± 0.7 | 77.5 | 6.4 ± 9.9 | 70.1 ± 10.1 | 78.3 ± 3.1 | 17.4 | 14.8 ± 2.8 | 17.1 ± 0.2 | 17.2 ± 0.1 |
| Medium-R       | 19.2 | 0.7 ± 0.6 | 6.5 ± 5.1 | 7.3 ± 1.3 | -0.3 | 8.5 ± 2.2 | 9.9 ± 2   | 18.6 ± 6.5 | 15.5 | 1.7 ± 0.4  | 1.6 ± 0.4  | 1.5 ± 0.3  |
| Medium-E       | 40.1 | -0.1 ± 0.1 | 1.5 ± 2.5 | 2.3 ± 2.2 | 76.9 | 20.6 ± 16.8 | 64.1 ± 10.8 | 77.5 ± 3.1 | 53.8 | 35.5 ± 10.4 | 52.5 ± 1.2 | 53.3 ± 0.3 |
|                |      |     |                 |                 |      |     |                 |                 |      |     |                 |                 |
| Random         | 4.9  | 1.8 ± 0.9 | 4.5 ± 0.5 | 4.8 ± 0.3 | 7    | 1.7 ± 1.3 | 3.2 ± 1.4 | 3.4 ± 1.9 | 13.6 | -0.2 ± 0.2 | -0.1 ± 0.1 | -0.1 ± 0.2 |
| Medium         | 53.1 | 32.8 ± 8.2 | 50.9 ± 4.3 | 52.3 ± 1.4 | 79.2 | 42.9 ± 24.2 | 80.1 ± 12 | 81.7 ± 3.1 | 17.8 | 7 ± 3.6   | 5.7 ± 4.7  | 11 ± 4.3  |
| Medium-R       | 15   | 6.9 ± 0.6 | 14.9 ± 0.2 | 15.1 ± 0.2 | 26.7 | 4.6 ± 3.9 | 0.8 ± 0.5 | 2 ± 1.5 | 39   | 5.1 ± 5.7  | 3.1 ± 2.4  | 14.2 ± 4.5 |
| Medium-E       | 57.5 | 32.5 ± 9.1 | 55.2 ± 3.8 | 57.2 ± 0.2 | 111  | 49.5 ± 26.7 | 63.5 ± 22.5 | 93.3 ± 8.8 | 44.6 | 5.3 ± 3.9  | 5.5 ± 3.5  | 17.2 ± 8.7 |
Table 24: Normalized scores for the D4RL tasks (with joint noise shift). We take the baseline results (for 10T) of MOPO from their original papers and that of the other model-free methods (BEAR, BRAC-p, AWR, BCQ and CQL) from the D4RL paper [Fu et al., 2020].

| Joint Noise Shift | Hopper | Walker2d |
|-------------------|--------|---------|
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |
|                   | Random | Medium | Medium-R | Medium-E |