High-temperature phase chemistry of the system Gd–Pd–O

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Abstract

An isothermal section of the phase diagram for the system Gd–Pd–O at 1223 K has been established by equilibration of samples and phase identification after quenching by optical and scanning electron microscopy, X-ray powder diffraction, and energy dispersive spectroscopy. Three ternary oxides Gd\textsubscript{2}PdO\textsubscript{5}, Gd\textsubscript{4}PdO\textsubscript{8} and Gd\textsubscript{4}Pd\textsubscript{2}O\textsubscript{4} were identified. Liquid alloys, the four inter-metallic compounds and Pd-rich solid solution were found to be in equilibrium with Gd\textsubscript{2}O\textsubscript{3}.

Based on the phase relations, four solid-state cells were designed to measure the Gibbs energies of formation of the three ternary oxides in the temperature range from 920 to 1320 K. Although three cells are sufficient to obtain the properties of the three compounds, the fourth cell was deployed to cross check the data. An advanced version of the solid-state cell incorporating a buffer electrode with yttria-stabilized zirconia solid electrolyte and pure oxygen gas at a pressure of 0.1 MPa as the reference electrode was used for high-temperature thermodynamic measurements. The standard Gibbs energy of formation of the inter-oxide compounds from their component binary oxides can be represented by the following equations:

\[ \Delta_{\text{f(ox)}}^{\text{G}}(\text{J mol}^{-1}) = -25,030 + 0.337T \]  \hspace{1cm} (±140), \hspace{1cm} \text{Gd}_2\text{PdO}_4(s): \Delta_{\text{f(ox)}}^{\text{G}}(\text{J mol}^{-1}) = -25,350 + 0.847T \]  \hspace{1cm} (±135),

\[ \Delta_{\text{f(ox)}}^{\text{G}}(\text{J mol}^{-1}) = -48,700 + 0.387T \]  \hspace{1cm} (±270)

Based on the thermodynamic information, isothermal chemical potential diagrams and isobaric phase diagrams for the system Gd–Pd–O are developed. © 2002 Elsevier Science Ltd. All rights reserved.

Keywords: Phase diagram; Gibbs energy; Enthalpy; Entropy; Gd\textsubscript{2}PdO\textsubscript{5}; Gd\textsubscript{4}PdO\textsubscript{8}; Gd\textsubscript{4}Pd\textsubscript{2}O\textsubscript{4}

1. Introduction

As a part of systematic studies on phase equilibria and thermodynamic properties of compounds in the ternary systems Re–X–O, where Re is a rare earth element and X is a metal from the platinum group, measurements have been made on the system Gd–Pd–O at high-temperatures. Some of the ternary oxides of this group have potential application in catalysis and electrochemistry. The compound Gd\textsubscript{2}PdO\textsubscript{4} exhibits three-way catalytic behavior for automobile exhaust clean-up, simultaneously aiding the oxidation of CO and the hydrocarbons and the reduction of NO [1]. To understand the behavior of the catalysts, it is useful to have information on the thermodynamic stability domain of the compound. Quantitative information on the stability of the ternary oxides is also useful for assessing the interaction of Pt-group metals with ceramic compounds containing rare earth elements under different environments. Furthermore, the thermodynamic data are beneficial for the design of processes for the recovery of rare earth and precious metals from scrap. Phase diagrams of higher order systems containing these elements can be readily computed from thermodynamic data on binary and ternary compounds.

Two stable ternary compounds, Gd\textsubscript{2}PdO\textsubscript{4} and Gd\textsubscript{4}Pd\textsubscript{2}O\textsubscript{5} were reported in the system Gd–Pd–O by McDaniel and Schneider [2]. Recently, Andersson et al. [3] have shown that Ln\textsubscript{2}PdO\textsubscript{4} compounds for Ln = La, Nd, Sm, Eu, and Gd can be indexed on a triclinic unit cell (space group \textit{P\text{\textsc{t}}}). The chains of PdO\textsubscript{4} squares are staggered, except in the case of La\textsubscript{2}PdO\textsubscript{4}. The lattice parameters of Gd\textsubscript{2}PdO\textsubscript{4} are \( a = 1.5795 \text{ nm}, b = 0.71142 \text{ nm}, c = 0.67853 \text{ nm}, \alpha = 95.723^\circ, \beta = 131.244^\circ, \gamma = 122.771^\circ. \) The compound Gd\textsubscript{4}Pd\textsubscript{2}O\textsubscript{5} decomposes to Gd\textsubscript{4}PdO\textsubscript{8}, Pd and O\textsubscript{2} in air at \( \sim 1298 \text{ K}, \) Gd\textsubscript{2}PdO\textsubscript{4} decomposes to Gd\textsubscript{4}Pd\textsubscript{2}O\textsubscript{5} and Gd\textsubscript{4}Pd\textsubscript{2}O\textsubscript{4} at \( \sim 1278 \text{ K}, \) according to McDaniel and Schneider [2].

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In this study, phase equilibria involving the oxide phases were first determined at 1223 K by isothermal equilibration and phase analysis of quenched samples. Based on the phase diagram, solid-state cells were designed to measure the Gibbs energies of formation of the ternary oxides. In general, the electrochemical method has been found simpler and superior to other techniques for the determination of Gibbs energies of formation of oxides [4]. Yttria-stabilized zirconia (YSZ) was used as the solid electrolyte and pure oxygen at a pressure of 0.1 MPa as the non-polarizable reference electrode. Errors in electrochemical measurements often arise from polarization of the electrodes, especially when they contain more than two phases. Because of the difference in the chemical potential of the mobile species between the reference and working electrodes of such cells, there is always a small flux through the electrolyte separating them, even in the absence of physical porosity [5]. The electrochemical permeability is caused by coupled transport of mobile ions and holes (or electrons) in the solid electrolyte under the chemical potential gradient. Used in this study was a buffer electrode, which absorbed the flux and prevented polarization of the measuring electrode. This new special feature and the use of the primary reference standard for oxygen chemical potential allowed the generation of accurate data on the ternary oxides.

2. Experimental

2.1. Materials

Reactive forms of Gd₂O₃ and PdO were used as the starting materials for the synthesis of the ternary oxides. The reactive binary oxides were prepared by the decomposition of the respective nitrates at reduced pressure (10 Pa); Gd(NO₃)₃·6H₂O at 1073 K and Pd(NO₃)₂ at 723 K. The inter-oxide compounds Gd₃PdO₇ and Gd₃Pd₂O₇ were prepared by heating pellets containing Gd₂O₃ and PdO in the appropriate ratio at 1300 K in dry oxygen for six days, with regrinding and recompaction at intervals of two days in a glove box. The pellets were then homogenized at 1350 K in pure dry oxygen for 12 h. The pellets, prepared from an intimate mixture of the components by compaction at 150 MPa using steel die, were contained in calcia crucibles and supported on sacrificial pellets of the same composition. The compound Gd₃PdO₇ was made by direct reaction of Gd₂O₃ and PdO at 1223 K in pure oxygen for two days. The pellet was ground to fine powder and then compacted again for further heat treatment for four days. The inter-metallics (GdPd, Gd₂Pd, Gd₃Pd₂, and GdPd₃) were prepared by the powder metallurgy route. The powders of the two pure metals, each of 99.9% purity, were mixed in the stoichiometric ratio, compacted at 150 MPa, placed in a closed Mo crucible, and heat-treated at 1275 K for four days in evacuated quartz ampoules. Placing titanium foil around the sample prevented oxidation during subsequent annealing in prepurified argon gas at 1350 K. The formation of inter-metallics and inter-oxide compounds was confirmed by XRPD. The lattice parameters of the inter-metallics and oxides were in good accord with values reported in the literature [3,6]. YSZ tubes and crucibles were obtained from Zircoa Corporation.

2.2. Determination of the phase diagram

The phase relations were explored by equilibrating mixtures of metals or inter-metallics with the different oxides at 1223 K, followed by quenching in liquid nitrogen or chilled mercury and phase identification. Thus, 16 compositions were equilibrated for periods up to 18 days; one along the binary Gd–O, and the rest inside the ternary. During this period, twice the samples were quenched, ground to ~325 mesh, and repelletized for further heat treatment. The phase compositions of the samples were unaltered by further heating. The average composition of the samples studied is shown by cross marks on the Gibbs triangle in Fig. 1.

Two arrangements were used for equilibrating samples at high-temperature. Several mixtures containing Gd₂O₃, PdO, and the inter-oxide compounds were equilibrated in pure oxygen at a pressure of 0.1 MPa, using an apparatus described earlier [7]. The samples were held in calcia crucibles, and kept on sacrificial disks of the same composition. The mass of each sample pellet was determined before and after equilibration. Sample pellets containing either pure metal or alloy were contained in closed Mo crucibles, which were sealed in evacuated quartz ampoules. To minimize physical contact between the pellet and the Mo crucible, the pellet was placed on a disk containing only the oxides. This precaution was taken to avoid contamination of

![Fig. 1. Isothermal section of the phase diagram for the system Gd–Pd–O at 1223 K. The average composition of the samples examined in this study is shown by the symbol X.](image)
the samples by molybdenum. In many cases, samples of the same overall composition were made, using different starting materials. Optical and scanning electron microscopy, EDS, and XRPD identified phases present in the quenched samples.

2.3. Measurement of Gibbs energies of formation of ternary oxides

The reversible emf of the following solid-state cells were measured as a function of temperature

\[ Pt, \text{Pd} + \text{Gd}_2\text{PdO}_3 + \text{Gd}_2\text{O}_3/(Y_2\text{O}_3)\text{ZrO}_2/O_2(0.1 \text{ MPa}), \text{Pt} \quad \text{Cell 1} \]

\[ Pt, \text{Pd} + \text{Gd}_2\text{PdO}_4 + \text{Gd}_2\text{PdO}_7/(Y_2\text{O}_3)\text{ZrO}_2/O_2(0.1 \text{ MPa}), \text{Pt} \quad \text{Cell 2} \]

\[ Pt, \text{Pd} + \text{Gd}_2\text{Pd}_2\text{O}_3 + \text{Gd}_2\text{Pd}_2\text{O}_7/(Y_2\text{O}_3)\text{ZrO}_2/O_2(0.1 \text{ MPa}), \text{Pt} \quad \text{Cell 3} \]

The cells were designed based on the phase relations established at 1223 K. During the course of the emf studies, it was found that the compound \( \text{Gd}_2\text{PdO}_4 \) decomposed above 1280 K. A new three-phase region involving \( \text{Pd, Gd}_2\text{PdO}_7 \) and \( \text{Gd}_2\text{Pd}_2\text{O}_3 \), thus came into existence at \( T \simeq 1280 \text{ K} \). Hence, the emf of a fourth cell:

\[ \text{Pt, Pd} + \text{Gd}_2\text{Pd}_2\text{O}_3 + \text{Gd}_2\text{Pd}_2\text{O}_7/(Y_2\text{O}_3)\text{ZrO}_2/O_2(0.1 \text{ MPa}), \text{Pt} \quad \text{Cell 4} \]

was measured from 1280 to 1320 K.

Two experiments were conducted on each cell. All the cells are written such that the right hand electrodes are positive. \( (Y_2\text{O}_3)\text{ZrO}_2 \) is an oxygen ion conductor with ionic transport number greater than 0.99 at the temperatures and oxygen partial pressures encountered in this study [4]. However, the presence of trace hole conduction in the electrolyte gives rise to a small electrochemical flux of oxygen from the reference electrode on the right side to the working electrodes on the left side of each cell [5]. The electrochemical permeability is caused by the coupled transport of oxygen ions and holes in the solid electrolyte under the oxygen potential gradient. Only opposing it with an external dc voltage, exactly equivalent to the oxygen chemical potential difference, can stop this flow of oxygen [8].

The electrochemical flux of oxygen would have caused polarization of the multphase solid electrodes. The chemical potential of oxygen in the microsystem near the solid electrode/electrolyte interface would have been altered because of the semipermeability of the electrolyte to oxygen. A buffer electrode, introduced between reference and working electrodes was designed to act as a sink for the oxygen flux and prevent the flux from reaching the working electrode. The buffer electrode was maintained at an oxygen chemical potential close to that of the working electrode. Since there was no significant difference between the chemical potentials of buffer and working electrodes, driving force for transport of oxygen through the zirconia tube separating these electrodes did not exist. The working electrode therefore remained unpolarized. Pure oxygen gas at a pressure of 0.1 MPa, flowing over a platinized surface of zirconia, constituted the primary reference standard for oxygen chemical potential and formed a non-polarizable electrode. Thus, the three electrode design of the cell prevented error in emf caused by polarization of the working electrode. Measuring separately the emf between the three electrodes, two at a time, assessed the magnitude of the polarization effect. Transport of oxygen between the electrodes through the gas phase was prevented by physical isolation of the gas phase over the three electrodes.

The cell design used for high-temperature emf measurements is shown in Fig. 2. It consisted of three distinct compartments, separated by two impervious YSZ tubes and a YSZ crucible. The cell can be represented schematically as follows:

| Working Electrode | Buffer Electrode | Reference Electrode |
|-------------------|------------------|---------------------|
| \( (Y_2\text{O}_3)\text{ZrO}_2 \) | \( \text{O}_2(\text{P}_{\text{O}_2}) \) | \( \text{O}_2(0.1 \text{ MPa}) \) |

\( \text{Pt} \)

The working and reference electrodes were contained inside separate zirconia tubes. The cell emf measured between the working and reference electrodes was determined only by the oxygen chemical potential at these electrodes and was not affected by the gradient of chemical potential through the connecting chain consisting of the solid electrolyte segments and the buffer electrode. Construction of the high-temperature galvanic cell was rendered more difficult by the introduction of the buffer electrode. Moreover, in some of the cells used in this study, the partial pressure of oxygen at the working electrode was quite appreciable, especially at the higher

![Fig. 2. A schematic diagram of the new apparatus for high-temperature emf measurements, with a buffer electrode interspersed between reference and working electrodes.](image-url)
temperatures. Therefore, the static sealed design used by Charette and Flengas [9] was found more appropriate than other designs that employ either dynamic vacuum or inert gas flow over the electrodes [4,10].

The working electrode consisted of a mixture of Pd + Gd$_2$PdO$_2$ + Gd$_3$O$_7$ in the ratio 1:1.5:1 in cell 1; a mixture of Pd + Gd$_2$PdO$_2$ + Gd$_4$PdO$_7$ in the ratio 1:1.5:1 in cell 2; a mixture of Pd + Gd$_2$PdO$_3$ + Gd$_4$PdO$_4$ in the ratio 1:1.5:1 in cell 3; a mixture of Pd + Gd$_2$PdO$_3$ + Gd$_4$PdO$_7$ in the ratio 1:1.5:1 in cell 4. In each case, an excess of the component that decomposed to establish the oxygen pressure in the closed system was taken. The average particle size of the powders used to prepare the working and buffer electrodes was in the range from 3 to 8 μm.

The details of cell assembly and operational procedures used in this study were identical with those reported elsewhere [11,12]. At the end of each experiment, the electrodes were cooled to room temperature and examined by optical and scanning electron microscopy and XRPD. Although small changes in the relative concentration of the constituents were observed in some cases, the number and nature of the phases remained unaltered. The change in relative concentration was consistent with the expected decomposition of one of the oxides at high temperature to generate the equilibrium oxygen pressure in sections of the apparatus.

Observed in preliminary experiments was cyclic fluctuation in emf at constant temperature; the magnitude was ±1.8 mV for cell 1. The resistance of the cell increased with time at 1300 K indicating the gradual formation of a non-conducting phase at the electrode/electrolyte interface. Careful examination of the interface using cross-sectional transmission electron microscopy (TEM) indicated localized islands of Gd$_2$Zr$_2$O$_7$. Physical contact of Gd$_3$O$_7$ in the electrode with the solid electrolyte was therefore avoided by coating the electrolyte surface with a thin layer of metal Pd. Painted on all surfaces of the solid electrolyte in contact with the working and buffer electrodes was a solution of PdCl$_2$. After firing in air at 1275 K, a thin film of Pd metal was obtained. The process was repeated three times to obtain a satisfactory coating on the whole contact surface. The Pd film on the electrolyte converts partly into tiny spheres when held at 1375 K for 2 h. With the introduction of the spherical Pd barrier at electrode/electrolyte interface, the fluctuation in emf decreased to ±0.2 mV. Hence, the Pd barrier was used in subsequent measurements on the different cells.

3. Results and discussion

3.1. Phase diagram

The isothermal section at 1223 K of the equilibrium phase diagram for the system Gd–Pd–O, composed from the results obtained by equilibration and phase identification of quenched samples by optical and scanning electron microscopy, EDS and XRPD, are shown in Fig. 1. Equilibrium was assumed when the XRPD or EDS showed no change after successive heat treatments. In several phase fields, equilibrium was confirmed by using different starting materials to produce samples of the same average chemical composition, and verifying that the samples had identical phase composition after equilibration. There was no difference in the phase composition of identical samples quenched into liquid nitrogen and chilled mercury.

Along the binary Pd–O, there was no stable oxide at 1223 K. Along the Gd–O binary, Gd$_2$O$_7$ was detected. A liquid phase was present along the Gd–Pd binary for $0.19 \leq x_{\text{Pd}} \leq 0.33$. Along the binary Gd–Pd, four intermetallics (GdPd, Gd$_3$Pd$_4$, Gd$_4$Pd$_2$ and ‘GdPd$_5$’) and Pd-rich solid solution were observed in addition to the liquid phase. The compound ‘GdPd$_5$’ is non-stoichiometric. These results are in general agreement with the phase diagram for Gd–Pd binary available in the literature [13]. All the three ternary oxides lie on the Gd$_2$O$_3$–PdO join. The ternary compounds were slightly non-stoichiometric, although their precise boundaries could not be established using EDS. The XRPD patterns of the oxides in different phase field were almost identical. The valence of Pd in all the oxides encountered in this study was two.

Metal Pd was found to be in equilibrium with Gd$_2$O$_3$ and the ternary oxide phases in different phase fields. Three three-phase fields involving Pd and the different ternary oxides were identified at 1223 K. Each of these phase fields involving three condensed phases is characterized by an unique oxygen potential at constant temperature and total pressure in accordance with the phase rule. Measurement of the oxygen partial pressure in the three-phase regions provides a means for determining the Gibbs energies of formation of the ternary oxides. Each of the three ternary oxides were stable in the presence of pure oxygen gas at 1223 K. The Gd–Pd liquid, inter-metallics and Pd-rich solid solution were found to be in equilibrium with Gd$_2$O$_3$.

3.2. Standard Gibbs energies of formation of ternary oxides

Polarization of the buffer electrode was small but significant in cells 1–4: the absolute value of the emf of the buffer electrode against the reference was 6–14 mV lower than that of the working electrode. The variation of the oxygen potential across the three electrode cell is shown in Fig. 3. The polarization effect ($E_p$) is given by:

$$E_p = E_{\text{ref}} - E_{\text{eb}} - E_{\text{b/w}}$$

where $E_{\text{ref}}$ is the correct emf of the cell measured between the unpolarized reference and working electrodes, $E_{\text{eb}}$ is the emf between the reference and buffer electrodes, and $E_{\text{b/w}}$ is the emf between the buffer and working electrodes. The emf across each solid electrolyte membrane is related to the oxygen potential difference across it. $E_p$ is the electrochemical equivalent of the oxygen potential gradient across the buffer electrode. The polarization effect was more
pronounced at high-temperatures. Thus, the need for the buffer electrode for accurate thermodynamic measurements was clearly demonstrated.

The reversible emfs of cells 1–4 are shown as a function of temperature in Fig. 4. The linear least-squares regression analysis of the emf of cell 1 in the temperature range from 920 to 1320 K gives,

\[ E_1/mV = 709.7 - 0.5089T(\pm 0.34) \]  

(2)

The uncertainty limit corresponds twice to the standard error estimate. The emf of cell 1 is related to the standard Gibbs energy of formation of Gd₂PdO₇ from Gd₂O₃, Pd and O₂ gas

\[ 2\text{Gd}_{2}\text{O}_{3}(s) + \text{Pd}(s) + 1/2\text{O}_{2}(g) \rightarrow \text{Gd}_{2}\text{PdO}_{7}(s) \]  

(3)

\[ \Delta_f(G^\circ)/J\text{ mol}^{-1} = -2FE_1 = -136,950 + 98.20T \]  

(4)

where \( F \) is the Faraday constant and \( \Delta_f(G^\circ) \) represents the standard Gibbs energy change for reaction (3). Gd₂O₃ used in this study had the cubic structure (space group \( Ia\bar{5} \)). The standard Gibbs energy of formation of PdO was determined recently [11]. For the formation of PdO

\[ \text{Pd}(s) + 1/2\text{O}_{2}(g) \rightarrow \text{PdO}(s) \]  

(5)

\[ \Delta_f(G^\circ)/J\text{ mol}^{-1} = -111,920 + 97.87T \quad (\pm 120) \]  

(6)

Hence, the Gibbs energy of formation of Gd₂PdO₇ from its component oxides can be obtained by combining Eqs. (4) and (6). For the reaction,

\[ 2\text{Gd}_{2}\text{O}_{3}(s, \text{C-Rare Earth}) + \text{PdO}(s) \rightarrow \text{Gd}_{2}\text{PdO}_{7}(s) \]  

(7)

\[ \Delta_f(G^\circ)/J\text{ mol}^{-1} = \Delta_f^\circ(G^\circ(\text{Gd}_{2}\text{PdO}_{7})) = -25,030 + 0.33T \]  

(8)

The temperature-independent term on the right hand side of Eq. (8) is the enthalpy of formation of Gd₂PdO₇ from component oxides at an average temperature of \( \sim 1120 \) K. The temperature-dependent term is related to the corresponding entropy of formation.

The emf of cell 2 was reproducible and varied linearly with temperature in the range 920–1280 K. The least-squares regression analysis gives,

\[ E_2/mV = 713.0 - 0.5141T \quad (\pm 0.44) \]  

(9)

The emf of cell 2 is related to the standard Gibbs energy change for the reaction

\[ \text{Gd}_{2}\text{PdO}_{7}(s) + \text{Pd}(s) + 1/2\text{O}_{2}(g) \rightarrow 2\text{Gd}_{2}\text{PdO}_{4}(s) \]  

(10)

\[ \Delta_f(G^\circ)/J\text{ mol}^{-1} = -2FE_2 = -137,590 + 99.21T \]  

(11)

(\( \pm 85 \))

Combining reactions (3), (5), and (10), one obtains the reaction representing the formation of Gd₂PdO₄ from its component oxides

\[ \text{Gd}_{2}\text{O}_{3}(s, \text{C-Rare Earth}) + \text{PdO}(s) \rightarrow \text{Gd}_{2}\text{PdO}_{4}(s) \]  

(12)
\[ \Delta_{f(12)} G^0 = \Delta_{f(03)} G^0 (\text{Gd}_2\text{PdO}_4) / \text{J mol}^{-1} = -25,350 + 0.847T \]
\((\pm 135)\) \hfill (13)

The measured emf of cell 3 can be expressed by the relation:
\[ E_3 / \text{mV} = 701.0 - 0.5048T \quad (\pm 0.5) \] \hfill (14)

At higher temperatures, Gd$_2$PdO$_4$ was found to decompose gradually to a mixture of Gd$_2$PdO$_7$ and Gd$_3$Pd$_2$O$_9$. Thus, the solid-state decomposition temperature of Gd$_2$PdO$_4$ is 1280 K and this temperature should be independent of oxygen partial pressure. The emf of cell 3 is related to the standard Gibbs energy change for the reaction:
\[ \text{Gd}_2\text{PdO}_4(s) + \text{Pd}(s) + 1/2\text{O}_2(g) \rightarrow \text{Gd}_3\text{Pd}_2\text{O}_9(s) \] \hfill (15)
\[ \Delta_{f(15)} G^0 / \text{J mol}^{-1} = -2F E_3 = -135,270 + 97.41T \]
\((\pm 100)\) \hfill (16)

The standard Gibbs energy of formation of Gd$_2$PdO$_7$ from its component oxides can be computed by combining the standard Gibbs energy changes associated with Eqs. (3), (5), (10) and (15):
\[ \text{Gd}_2\text{O}_3(s, \text{C-Rare Earth}) + 2\text{PdO}(s) \rightarrow \text{Gd}_3\text{Pd}_2\text{O}_9(s) \] \hfill (17)
\[ \Delta_{f(17)} G^0 = \Delta_{f(03)} G^0 (\text{Gd}_2\text{PdO}_3) / \text{J mol}^{-1} \]
\[ = -48,700 + 0.387T \quad (\pm 270) \] \hfill (18)

Above 1280 K, a three-phase region involving Pd, Gd$_2$PdO$_7$ and Gd$_3$Pd$_2$O$_9$ was found to emerge. Cell 4 measured the oxygen potential in this three-phase field. The emf of cell 4 can be expressed by the relation:
\[ E_4 / \text{mV} = 704.5 - 0.5075T \quad (\pm 0.35) \] \hfill (19)

The emf of cell 4 was obtained only in a limited temperature range from 1280 to 1320 K. The emf of cell 4 is related to the standard Gibbs energy change for the reaction:
\[ \text{Gd}_4\text{PdO}_7(s) + 3\text{Pd}(s) + 3/2\text{O}_2(g) \rightarrow 2\text{Gd}_3\text{Pd}_2\text{O}_9(s) \] \hfill (20)
\[ \Delta_{f(20)} G^0 / \text{J mol}^{-1} = -6F E_4 = -407,840 + 293.80T \]
\((\pm 200)\) \hfill (21)

This result can be independently calculated from the emfs of cells 2 and 3:
\[ \Delta_{f(20)} G^0 / \text{J mol}^{-1} = -2F (E_2 + E_3) \]
\[ = -408,130 + 294.03T \quad (\pm 210) \] \hfill (22)

Both methods give almost identical results for the Gibbs energy in the temperature range of measurement. Although such good agreement may be fortuitous, it clearly demonstrates the internal consistency of the emf data.

The emf of cell 4 was identical to that of cells 2 (54.9 mV) at 1280 K. However, the values of the decomposition temperature of Gd$_3$PdO$_9$ obtained by solving the three equations for emf, in binary combinations, are slightly different. The emf of cells 2 and 3 intersect at 1290 K, cells 2 and 4 at 1288 K, and cells 3 and 4 at 1296 K.

Without the use of the buffer electrode, the measured emf would have been lower by 6–14 mV for each cell involving a three-phase electrode. Because of polarization, the measured Gibbs energies of formation would have been more positive. The reference electrode used in this study (pure O$_2$ at 0.1 MPa) is non-polarizable. When polarizable reference electrodes are used, it is necessary to introduce another buffer electrode with almost identical chemical potential adjacent to the reference. In the absence of a driving force, there would then be no oxygen flux through the solid electrolyte membrane separating the reference electrode and its buffer under open circuit conditions. Consequently, the reference electrode would be protected from polarization. Thus, polarization would be confined to the two buffer electrodes.

The dissociation temperature of the compounds in air computed from the thermodynamic data obtained in this study can be compared with values reported in the literature [2], which are probably associated with an uncertainty of 10–15 K. Table 1 indicates that the dissociation temperature of Gd$_2$Pd$_3$O$_5$ in air obtained from the results of this study is in good agreement with the values reported by McDaniel and Schneider [2]. The values for the solid-state decomposition temperature of Gd$_3$PdO$_9$ obtained in the two studies are also in fair agreement. McDaniel and Schneider [2] did not identify the compound Gd$_3$PdO$_7$. The literature does not contain any thermodynamic information on the ternary oxides for comparison with the results obtained in this study.

The Gibbs energy of mixing for the system Gd$_3$O$_3$–PdO at 1223 K is shown in Fig. 5 as a function of composition. The value of the Gibbs energy of mixing for each compound is obtained by dividing its standard molar Gibbs energy of formation from the component binary oxides by the number of molecules of the binary oxides present in the compound. The minimum in the Gibbs energy of mixing occurs at the 1:2 composition corresponding to the compound Gd$_3$Pd$_2$O$_9$. The enthalpy of mixing also has a similar shape since entropies of formation of all the ternary compounds from Gd$_3$O$_3$,

| Compound     | Dissociation temperature (T, K) | Reference |
|--------------|---------------------------------|-----------|
| Gd$_2$PdO$_7$| 1308 (±1)                       | 1395 (±1) | This study |
| Gd$_3$PdO$_7$| 1278 (±15)                      | –         | [2]       |
| Gd$_3$Pd$_2$O$_9$ | 1280 (±5)                  | 1280 (±5) | This study |
| Gd$_3$Pd$_2$O$_9$ | 1298 (±10)                 | –         | [2]       |
| Gd$_3$Pd$_2$O$_9$ | 1302 (±1)                 | 1389 (±1) | This study |

* Solid-state decomposition to Gd$_3$PdO$_7$ and Gd$_3$Pd$_2$O$_9$. 
and PdO are numerically small and have the same sign. All the ternary oxides are primarily stabilized by their large negative enthalpies of formation.

The standard Gibbs energy of formation of the ternary oxides from elements can be readily calculated as a function of temperature in the range 920 \( \leq T \leq 1320 \) K using the results obtained in this study and values for the Gibbs energy of formation of cubic Gd\(_2\)O\(_3\) from the compilation of Pankratz [14]. The calculated values are given in Table 2 along with the standard Gibbs energy of Gd\(_2\)O\(_3\). For each compound, the data are represented by linear equations. Using the Neumann–Kopp rule to estimate the heat capacity of the ternary oxides relative to their constituent binary oxides, thermodynamic properties of the ternary oxides at 298.15 K can be evaluated. The standard enthalpies and entropies of formation of the three inter-oxide compounds from component binary oxides and from elements, and their standard entropies are listed in Table 3. The thermodynamic data for Gd (\(S^0_{298.15}/\text{J mol}^{-1} \text{K}^{-1} = 67.95\)), O\(_2\) (\(S^0_{298.15}/\text{J mol}^{-1} \text{K}^{-1} = 205.037\)), Pd (\(S^0_{298.15}/\text{J mol}^{-1} \text{K}^{-1} = 37.71\)) and Gd\(_2\)O\(_3\) (\(S^0_{298.15}/\text{J mol}^{-1} \text{K}^{-1} = 150.624\); \(H^0_{298.15}/\text{kJ mol}^{-1} = -1826.9\)) from Pankratz [14], and PdO (\(S^0_{298.15}/\text{J mol}^{-1} \text{K}^{-1} = 37.25\); \(H^0_{298.15}/\text{kJ mol}^{-1} = -115.51\) obtained from Ref. [11] were used.

### 3.3. Chemical potential diagrams

The oxygen chemical potential diagram for the system Gd–Pd–O at 1223 K, computed from the results of this study is shown in Fig. 6. The composition variable is cationic fraction, \(\eta_{\text{Pd}}(\eta_{\text{Gd}} + \eta_{\text{O}})\), where \(\eta_i\) represents moles of component \(i\). Since oxygen is not included in the composition parameter, information on oxygen non-stoichiometry cannot be displayed on the diagram. Nevertheless, the diagram provides useful information on the oxygen potential range for the stability of the various phases. The diagram is complimentary to the conventional Gibbs triangle representation of phase relations in ternary systems (see Fig. 1 as an example), where the composition of each phase can be unambiguously displayed. All the topological rules of construction for conventional temperature-composition phase diagrams are applicable to the oxygen potential diagram shown in Fig. 6.

When three condensed phases coexist at equilibrium in a ternary system such as Gd–Pd–O, the system is bivariant; at a fixed temperature and total pressure, three condensed phases coexist only at a unique partial pressure of oxygen. Therefore, horizontal lines on the diagram represent three-phase equilibria. On reducing the oxygen partial pressure at 1223 K, Gd\(_2\)Pd\(_2\)O\(_5\) dissociates first at \((P_{\text{O}_2}/P^0) = -1.378\), where \(P^0 = 0.1\) MPa is the standard atmospheric pressure. This is followed by the decomposition of Gd\(_2\)Pd\(_2\)O\(_4\) at a slightly reduced pressure, \((P_{\text{O}_2}/P^0) = -1.389\). The compound Gd\(_2\)Pd\(_2\)O\(_4\) is the last ternary oxide to decompose \((P_{\text{O}_2}/P^0) = -1.439\) on reducing the oxygen partial pressure. The oxygen potentials corresponding to the equilibria between alloys/inter-metallics and the gadolinium sesqui-oxide are computed using data for the oxide Gd\(_2\)O\(_3\) from Pankratz [14] and estimated data for Gd–Pd alloys, which are listed in Tables 2 and 4, respectively. The estimated data

Table 2
The standard Gibbs energies of formation of Gd\(_2\)O\(_3\), Gd\(_2\)Pd\(_2\)O\(_5\), Gd\(_2\)Pd\(_2\)O\(_4\), and Gd\(_2\)Pd\(_2\)O\(_3\) from elements

| Compound     | \(\Delta_{\text{f}}G^0/\text{J mol}^{-1}\) (920–1320 K) |
|--------------|--------------------------------------------------------|
| Gd\(_2\)O\(_3\) | -1.815,850 + 276.24T (±0.4040)                         |
| Gd\(_2\)Pd\(_2\)O\(_5\) | -3.768,650 + 650.68T (±0.8080)                         |
| Gd\(_2\)Pd\(_2\)O\(_4\) | -1.953,120 + 374.95T (±0.4040)                         |
| Gd\(_2\)Pd\(_2\)O\(_3\) | -2.088,390 + 472.36T (±0.4040)                         |

Table 3
Thermodynamic properties of Gd\(_2\)Pd\(_2\)O\(_5\), Gd\(_2\)Pd\(_2\)O\(_4\), and Gd\(_2\)Pd\(_2\)O\(_3\) at 298.15 K

| Compound     | \(\Delta_{\text{f}}G^0/\text{J mol}^{-1}\) | \(\Delta_{\text{f}}H^0/\text{J mol}^{-1}\) | \(\Delta_{\text{f}}S^0/\text{J mol}^{-1} \text{K}^{-1}\) | \(\Delta_{\text{f}}H^0/\text{J mol}^{-1} \text{K}^{-1}\) | \(\Delta_{\text{f}}S^0/\text{J mol}^{-1} \text{K}^{-1}\) | \(\Delta_{\text{f}}S^0/\text{J mol}^{-1} \text{K}^{-1}\) |
|--------------|----------------------------------------|----------------------------------------|----------------------------------------|----------------------------------------|----------------------------------------|----------------------------------------|
| Gd\(_2\)Pd\(_2\)O\(_5\) | -25.03 (±0.48)                         | -3794.34 (±10.01)                      | -0.33 (±0.48)                          | -689.14 (±1.78)                       | 338.17 (±0.87)                        |
| Gd\(_2\)Pd\(_2\)O\(_4\) | -25.35 (±0.48)                         | -1967.76 (±5.02)                      | -0.84 (±0.47)                          | -396.82 (±0.99)                       | 187.04 (±0.69)                        |
| Gd\(_2\)Pd\(_2\)O\(_3\) | -48.70 (±0.96)                         | -2106.62 (±5.10)                      | -0.38 (±0.96)                          | -499.51 (±1.31)                       | 224.75 (±1.29)                        |
for the Gd–Pd alloys were based primarily on calorimetric data of Guo and Kleppa [15], adjusted for consistency with phase relations obtained in this study. Similar oxygen potential diagrams at other temperatures, that may be required to address specific applications, can be readily computed from the thermodynamic data. Phase relations can also be computed as a function of temperature at constant oxygen partial pressure; plots for \((P_{O2}/P)^{\text{a}} = 1.0\) and 0.21 are shown in Fig. 7(a) and (b), respectively. It is apparent that the phase diagram is very sensitive to the partial pressure of oxygen.

It is interesting to view the stability of the various phases as a function of the chemical potentials of the three components. A three-dimensional representation at 1223 K is displayed in Fig. 8(a). The stability domain of each stoichiometric phase is defined by a plane, because the sum of the chemical potentials of the different components weighted by the appropriate stoichiometric coefficients is equal to the Gibbs energy of formation of the phase. Since the Gibbs energies of the alloy phases are functions of composition, they appear as a curved surfaces on the diagram. The stability of Gd$_2$PdO$_4$ and Gd$_4$PdO$_7$ are very restricted at 1223 K. In Fig. 8(a), the phases are represented as lines (planes with almost zero width). An expanded view with a little better resolution of stability domain of Gd$_2$PdO$_4$ and Gd$_4$PdO$_7$ is

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Fig. 6. Oxygen potential diagram for the system Gd–Pd–O at 1223 K.

Fig. 7. Isobaric phase diagrams for the system Gd–Pd–O: (a) \((P_{O2}/P)^{\text{a}} = 1.0\) and (b) \((P_{O2}/P)^{\text{b}} = 0.21\), where \(P^0\) is the standard atmospheric pressure (0.1 MPa).
Fig. 8. (a) Three-dimensional chemical potential diagram for the system Gd–Pd–O at 1223 K. Surfaces represent the stability domains of the various condensed phases as a function of the chemical potentials of the three components. (b) An expanded view of stability region of ternary oxides.

| Phase        | Gibbs energy of mixing, ΔG°^{mix}(g at)⁻¹ | Reference states |
|--------------|-------------------------------------------|------------------|
| GdPd         | −77.365 + 1.187T                          | Solid Pd, Gd     |
| Gd₂Pd₄        | −83.150 + 3.487T                          | Solid Pd, Gd     |
| GdPd₂         | −86.065 + 7.947T                          | Solid Pd, Gd     |
| GdPd₃         | −79.700 + 5.477T                          | Solid Pd, Gd     |
| Liquid alloy  | R_q(GdPd) ln X_p + 2 ln X_{Gd} + 160 ln X_{Pd} + 375 ln X_{O} | Liquid Pd, Gd    |
| Solid solution (Pd-rich) | R_q(GdPd) ln X_p + 2 ln X_{Gd} + 120 ln X_{Pd} + 350 ln X_{O} | Solid Pd, Gd     |

Displayed in Fig. 8(b). Lines, defined by the intersection of the planes or surfaces, represent two-phase fields. Points of intersection of three planes or surfaces identify three-phase equilibria. It is seen that the stability domains of the ternary oxides are restricted to the top right corner of the diagram, where the activity of Pd and the partial pressure of oxygen have relatively large values and the activity of Gd is very low. In reducing atmospheres Gd₂Pd₅O₇ can decompose to nanocrystalline Pd on microcrystalline Gd₂O₃ as reported by Andersson et al. [1]. The nanocrystalline Pd can act as a three-way catalyst for the conversion of CO, NO, and propene simultaneously to CO₂, N₂ and H₂O [16]. The ternary oxide has two roles: it functions as the precursor for in situ generation of nanocrystalline Pd on Gd₂O₃, and as the oxidation product that can easily regenerate the
catalyst in finely divided form by heat treatment in reducing atmospheres.

4. Conclusions

Isothermal section of the phase diagram of the system Gd–Pd–O at 1223 K has been established by phase analysis of samples quenched after equilibration at high-temperature. Three ternary oxides, Gd₃PdO₇, Gd₂PdO₄ and Gd₃Pd₂O₇ were found to be stable. Based on the phase diagram, three solid-state cells were designed to measure the chemical potential of oxygen corresponding to three separate phase fields in the ternary, each involving three condensed phases. During the course of the measurements, it was found that Gd₃PdO₄ decomposes to Gd₂PdO₇ and Gd₂Pd₂O₇ at 1280 K. Hence a fourth cell was designed to measure the oxygen potential in the three-phase field Pd + Gd₂PdO₇ + Gd₂Pd₂O₇. The emf measurements were conducted from 920 to 1320 K against the primary reference standard for oxygen potential. The advanced design of the solid-state cell used in this study incorporating a buffer electrode was used. Introducing a thin layer of Pd in spherical form at the electrode/electrolyte interface minimized interaction between Gd₂O₃ and (Y₂O₃) ZrO₂ electrolyte. These novel features enhanced the accuracy of thermodynamic data. The Gibbs energy changes corresponding to the following reactions were directly measured:

\[
\Delta G^\circ/J \text{ mol}^{-1} = -136,950 + 98.20T \quad (\pm 70)
\]

2Gd₂O₃(s, C-Rare Earth) + Pd(s) + 1/2O₂(g) → Gd₄PdO₇(s)

\[
\Delta G^\circ/J \text{ mol}^{-1} = -137,590 + 99.21T \quad (\pm 85)
\]

Gd₄PdO₇(s) + Pd(s) + 1/2O₂(g) → 2Gd₂PdO₄(s)

\[
\Delta G^\circ/J \text{ mol}^{-1} = -135,270 + 97.41T \quad (\pm 100)
\]

Gd₄PdO₇(s) + 3Pd(s) + 3/2O₂(g) → 2Gd₂Pd₂O₅(s)

\[
\Delta G^\circ/J \text{ mol}^{-1} = -407,840 + 293.80T \quad (\pm 200)
\]

From accurate measurements on cells incorporating buffer electrodes, the Gibbs energies, enthalpies and entropies of formation of the ternary oxides Gd₄PdO₇, Gd₂PdO₄, and Gd₃Pd₂O₇ were deduced for the first time. Chemical potential diagrams including a three-dimensional representation for the system Gd–Pd–O at 1223 K were developed based on the thermodynamic data obtained in this study and auxiliary information from the literature.

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