First hyperfine resolved far-infrared OH spectrum from a star-forming region*,**

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ABSTRACT

OH is an important molecule in the H2O chemistry and the cooling budget of star-forming regions. The goal of the Herschel key program “Water In Star-forming regions with Herschel” (WISH) is to study H2O and related species during protostellar evolution. Our aim in this Letter is to assess the origin of the OH emission from star-forming regions and constrain the properties of the emitting gas. High-resolution observations of the OH 1837.8 GHz (163.1 μm) towards the high-mass star-forming region W3 IRS 5 with the Heterodyne Instrument for the Far-Infrared (HIFI) on Herschel reveal the first hyperfine velocity-resolved OH far-infrared spectrum of a star-forming region. The line profile of the OH emission shows two components: a narrow component (FWHM ≈ 4–5 km s⁻¹) with partially resolved hyperfine structure resides on top of a broad (FWHM ≈ 30 km s⁻¹) component. The narrow emission agrees well with results from radiative transfer calculations of a spherical envelope model for W3 IRS 5 with a constant OH abundance of xOH ≈ 8 × 10⁻⁶. Comparison with H2O yields OH/H2O abundance ratios of around 10⁻³ for T ≳ 100 K and around unity for T < 100 K, consistent with the current picture of the dense cloud chemistry with freeze-out and photodesorption. The broad component is attributed to outflow emission. An abundance ratio of OH/H2O ≥ 0.028 in the outflow is derived from comparison with results of water line modeling. This ratio can be explained by a fast J-type shock or a slower UV-irradiated C-type shock.

Key words. astrochemistry – stars: formation – ISM: magnetic fields – ISM: jets and outflows – ISM: individual objects: W3 IRS 5

1. Introduction

Newly-formed stars inject large amounts of energy into the ambient interstellar material through shocks and radiation, heating the surrounding gas and dust. In these warm regions, H2O becomes one of the most abundant gas-phase molecules because water ice evaporates from the grain mantles and gas-phase formation routes become available. The hydroxyl radical (OH) is closely linked to both the H2O formation and destruction through OH + H → H2O + H as well as a byproduct of the H2O photodissociation process in the presence of UV photons. A significant fraction of the gas cooling occurs through line emission in the far-infrared, including lines of [O i], [C ii], CO, H2O, and OH (Gianinni et al. 2001; van Kempen et al. 2010).

Observations of the OH far-infrared transitions first became possible with the Kuiper Airborne Observatory

* Herschel is an ESA space observatory with science instruments provided by European-led Principal Investigator consortia and with important participation from NASA.

** Appendices are available in electronic form at http://www.aanda.org

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2\ kpc (Hachisuka et al. 2006) with a total luminosity of $\sim 10^3 \ L_\odot$ (e.g. Helmic & van Dishoeck 1997; Boonman et al. 2003; van der Tak et al. 2005; Chavarría et al. 2010; Benz et al. 2010).

2. Observations and data reduction

The OH triplet at 1837.747, 1837.817, and 1837.837 GHz from W3 IRS 5 was observed with HIFI on Herschel. The observations were carried out as part of the “Water In Star-Forming Regions with Herschel” (WISH) key program (van Dishoeck et al. 2011). W3 IRS 5 was observed on July 29th 2010 (obsid 1342201666) in dual beam switch mode with an on-source integration time of 17 min. The beam size (HPBW) at 1837 GHz is about 12\". The average system temperature was 1245 K. The wide band spectrometer (WBS) offers a nominal resolution of 1.1 MHz, corresponding to a velocity resolution of about 0.18 km s$^{-1}$ at 1837 GHz. The OH triplet at 1834.7 GHz was not observed.

HIFI clearly detects the OH triplet at around 1837.8 GHz with half the dual-sideband continuum. The expected positions of the lines and the source velocity are labeled. The blue lines show the best fit from the slab models and the outflow component separately.

Table 1. Molecular data of the observed OH transitions between the $^2\Pi \rightarrow 3/2$ and $1/2$ excited states.

| Transition | Frequency [GHz] | $A_\pi$ | $g_u$ | $g_v$ | Shift [km s$^{-1}$] |
|------------|-----------------|--------|------|------|------------------|
| 1$\rightarrow$1 | 1837.7466 | 2.1(−2) | 3 | 3 | 11.5 |
| 2$\rightarrow$1 | 1837.8168 | 6.4(−2) | 5 | 3 | 0.0 |
| 1$\rightarrow$0 | 1837.8370 | 4.3(−2) | 3 | 1 | −3.3 |

Notes: $A(B) = A \times 10^6$. The last column denotes the velocity shift relative to the component with the largest Einstein $A$ coefficient.

3. Results

HIFI clearly detects the OH triplet at around 1837.8 GHz (163.1 \mu m) towards W3 IRS 5 (Fig. 1). For the first time, the hyperfine components of the line triplet are spectrally resolved.

Two components dominate the line shape: the line profile shows narrow components residing on top of a broad emission feature, similar to that found by Chavarría et al. (2010) for H$_2$O lines in W3 IRS 5 and Kristensen et al. (2010) in low-mass YSOs. The narrow components with full widths at half maximum (FWHM) of $\sim 4$–5 km s$^{-1}$ are centered close to the positions expected from the hyperfine pattern. The lines are split by 20.2 MHz (3.3 km s$^{-1}$) towards the blue and 70.2 MHz (11.5 km s$^{-1}$) towards the red relative to the middle line. Therefore, the $(F = 2 \rightarrow 1 \rightarrow 1)$ transition is resolved. The underlying broad component with a FWHM of $\sim 30$ km s$^{-1}$ consists of the three blended hyperfine components, each with $\Delta v \sim 20$ km s$^{-1}$. The hyperfine pattern is unresolved in the broad component.

3.1. Slab models

As a first modeling step to derive OH column densities, the slab method outlined in Bruderer et al. (2010, Appendix B) is used. This method calculates the molecular spectrum from two slabs – one representing the envelope and one the outflow – in front of a continuum source, determined from the observed continuum flux. The slabs are assumed to cover the entire continuum source. The free parameters describing each slab are the OH column density $N_\text{OH}$, the excitation temperature $T_\text{ex}$ (assumed to be equal for all hyperfine transitions), the line width $\Delta v$, and the position of the line center $v_\text{lsr}$. Overlap between different hyperfine components of OH is taken into account. To constrain the free parameters ($N_\text{OH}$, $T_\text{ex}$, $\Delta v$, and $v_\text{lsr}$), the $\chi^2$ between observation and model is minimized using an uncertainty of $T_\text{rms} \sim 0.1$ K.

References:

1. http://www.iram.fr/IRAMFR/GILDAS
2. http://www.strw.leidenuniv.nl/~moldata/
3. http://spec.jpl.nasa.gov
The resolved hyperfine triplet structure of the narrow (envelope) component allows us to constrain the column density and the excitation temperature of the emitting gas simultaneously. Results of the best fitting slab models for the narrow component with a reduced $\chi^2 = 1.2$ are presented in Table 2. A peak line opacity of $\tau = 1.8$ is reached (2$+ \rightarrow$ 1$-$ transition) and the 1$+ \rightarrow$ 0$-$ and 1$+ \rightarrow$ 1$-$ peaks have optical depths of $\tau = 0.8$ and $\tau = 0.4$, respectively. Figure C.1 of the Appendix shows the 1$\sigma$ and 2$\sigma$ contours for the column density and excitation temperature. The OH column densities within the 1$\sigma$ interval range from $N_{\text{OH}} \approx 2 \times 10^{15} \text{ cm}^{-2}$, depending on $T_{\text{ex}}$, and thus vary by almost two orders of magnitude.

A broad (outflow) component can be clearly identified in the spectrum, but its hyperfine components are not resolved. Thus, it is not possible to determine an excitation temperature of the broad emission from the spectrum. Assuming $T_{\text{ex}} = 100$ K, a column density of $N_{\text{OH}} = 2.0 \times 10^{12} \text{ cm}^{-2}$ is obtained by fitting the line wings only. A lower limit on the OH column density of $N_{\text{OH}} \geq 7.2 \times 10^{13} \text{ cm}^{-2}$ is derived by assuming that the excitation temperature is equal to the upper level energy (270 K) of the transition. Both fits yield a line width of $\Delta v = 21.9 \text{ km s}^{-1}$ and a line position $v_{\text{lsr}} = -35.7 \text{ km s}^{-1}$. The line optical depth is $\tau < 0.01$ for these excitation temperatures. An optical depth of $\tau = 1$ is reached for $T_{\text{ex}} < 34$ K and no good fit can be obtained for $T_{\text{ex}} \lesssim 32$ K. In the following, $T_{\text{ex}} = 270$ K is assumed.

Table 2. Beam-averaged column density $N_{\text{OH}}$, excitation temperature $T_{\text{ex}}$, line width $\Delta v$, and line position $v_{\text{lsr}}$ of the best fit slab model.

| $N_{\text{OH}}$ [cm$^{-2}$] | $T_{\text{ex}}$ [K] | $\Delta v$ [km s$^{-1}$] | $v_{\text{lsr}}$ [km s$^{-1}$] | fit range [km s$^{-1}$] |
|--------------------------|-----------------|-----------------|-----------------|-----------------|
| O                        | 270.0           | 72.1            | -35.7           | [-60, -47.5], [-22, -10] |
| E                        | 3.9(16)         | 3.3             | -37.7           | [-43, -35], [-30, -23] |

Notes. $^{(a)}$ Fixed (see text). $A(B) \equiv A \times 10^8$. O = outflow, E = envelope.

To convert the column density into an OH abundance in the outflow, the $^{15}$CO(3–2) observation of Hasegawa et al. (1994) is used to derive $N_{\text{H}} = 1.3 \times 10^{22} \text{ cm}^{-2}$ with RADEX (van der Tak et al. 2007), assuming a CO/H$_2$ abundance ratio of $10^{-4}$, a density of $10^6 \text{ cm}^{-3}$, and a temperature of 60 K, as derived in their paper. This H$_2$ column density converts the lower limit of $N_{\text{OH}} \geq 7.2 \times 10^{13} \text{ cm}^{-2}$ into a lower limit on the OH abundance of $x_{\text{OH}} = N_{\text{OH}}/N_{\text{H}} \geq 5.5 \times 10^{-8}$.

3.2. Spherical model of the envelope

In addition to the slab modeling, the narrow emission component is compared to the results from full radiative transfer models using the “RATRAN” code (Hogerheijde & van der Tak 2000). The physical structure of W3 IRS 5 is taken from van der Tak et al. (2000) with a power-law density profile ranging from $n = 10^5$–$10^8 \text{ cm}^{-3}$ and temperatures of $50 \leq T \leq 950$ K within the Herschel beam at 1837 GHz. Dust and gas temperatures are assumed to be equal. Far-infrared extinction by the dust continuum for $T_{\text{dust}}$ is included. We also adopt their distance (2.2 kpc) for consistency. Dust opacities based on grains with thin ice mantles are assumed (Ossenkopf & Henning 1994, Table 1, Col. 5). The molecular abundance is assumed to be constant throughout the envelope, because this is the simplest structure yielding a good fit to the line profiles. Figure 2 shows the comparison between model and data, where the best fitting slab model for the broad component (cf. Sect. 3.1) is subtracted from the observation, leaving only the narrow component for a simpler comparison.

Fig. 2. Resulting HIIF spectrum after subtraction of the best fit outflow component. Overplotted are the spherical envelope models for constant OH abundances of $1 \times 10^{-8}$ (blue dashed), $8 \times 10^{-9}$ (red solid with individual components red dotted) and $5 \times 10^{-9}$ (pink dashed). Hyperfine components were simply added (see text).

Models assuming an OH abundance of $x_{\text{OH}} = (0.5–1) \times 10^{-7}$ agree reasonably well with the observed narrow components. RATRAN does not treat line overlap and overlap effects can therefore not be treated accurately for optically thick lines. Thus, we have simply added the intensities of the components as would be appropriate in the optically thin limit.

The spherical envelope models are also consistent with the 79, 84, and 119 $\mu$m lines being in absorption, as observed in the unpublished spectral scan obtained with PACS on Herschel. The 79 and 119 $\mu$m transitions are connected to the ground $^2\Pi_{3/2}$ level and therefore prone to absorption. A quantitative analysis is not possible because the central spatial pixel of the detector is saturated.

4. Discussion

Insight into the water chemistry can be gained by comparing OH and H$_2$O abundances, because these species are linked through the OH + H$_2$ ⇌ H$_2$O + H reactions. Chavarría et al. (2010) identify broad and narrow components in H$_2$O line profiles from W3 IRS 5 similar to OH. OH/H$_2$O abundance ratios can be derived separately for gas of the envelope and the outflow.

From the spherical non-LTE envelope models, which do not consider overlap of hyperfine components, we find an OH abundance of $x_{\text{OH}} \approx 8 \times 10^{-9}$ for W3 IRS 5. New calculations of the H$_2$O abundance $x_{\text{H}_2\text{O}}$ in the envelope, based on the work by Chavarría et al. (2010) but recalculated using the same physical structure as for OH, yield $x_{\text{H}_2\text{O}} = 10^{-5}$ for $T \geq 100$ K and $x_{\text{H}_2\text{O}} = 10^{-8}$ for $T < 100$ K. This allows us to estimate the OH/H$_2$O abundance ratios: H$_2$O is about three orders of magnitude more abundant in the inner envelope ($T \geq 100$ K), while the OH/H$_2$O ratio is around unity in the outer part ($T < 100$ K). The same conclusion is reached in the best fit H$_2$O abundance structure of Boonman et al. (2003) to ISO and SWAS data, which was derived with the same physical model as adopted here.

The inferred OH/H$_2$O ratios in the envelope are consistent with the current picture of the water chemistry in dense clouds (for detailed discussion of processes see Hollenbach et al. 2009; van Dishoeck et al. 2011). Different paths can increase the gas-phase H$_2$O abundance in the inner part of protostellar envelopes.
At $T \geq 100$ K, H$_2$O starts to evaporate from the ice mantles of dust grains. When temperatures of $T \gtrsim 230$ K are reached, which are typical for the innermost parts of high-mass protostellar envelopes, H$_2$O can be rapidly formed in the gas phase through OH + H$_2$ $\Rightarrow$ H$_2$O + H. In this case, OH is only a transient step of the H$_2$O formation process and thus OH/H$_2$O $\ll 1$ in the absence of UV photons. In the outer envelope, low-temperature gas-phase chemistry provides $x_{\text{OH}} \approx 10^{-8}$ (Doty et al. 2002, Fig. 1). At the outer edge, H$_2$O and OH can be released into the gas phase by photodesorption from grain mantles. Öberg et al. (2009) and Andersson & van Dishoeck (2008) find from laboratory data and theoretical calculations that roughly equal amounts of OH and H$_2$O are released at low temperatures. Depending on the optical depth of the lines, this outer layer may dominate the emission.

The slab model method outlined in Sect. 3.1 is also used to estimate the H$_2$O abundance in the outflow component. Availability of HIFI para-H$_2$O $2_0J-1_1K$ (from Chavarría et al. 2010) and unpublished $2_1J-2_0J$ (Chavarría et al., in prep.) and $3_1J-4_0J$ data allows us to constrain $N_{\text{H}_2\text{O}}$ and the para-H$_2$O excitation temperature in the outflow simultaneously. We find $N_{\text{H}_2\text{O}} = 6.4 \times 10^{14}$ cm$^{-2}$ and thus $N_{\text{H}_2O} = 2.6 \times 10^{15}$ cm$^{-2}$ for an assumed ortho-to-para H$_2$O ratio of 3:1. The water abundance is calculated to be $2.1 \times 10^{-6}$ with $N_{\text{H}_2}$ = $1.25 \times 10^{21}$ cm$^{-2}$. Under the assumption that the OH and H$_2$O emission arise from the same gas, we can calculate a lower limit of 0.028 on the OH/H$_2$O abundance ratio in the outflow of W3 IRS 5. This limit is consistent with the emission originating in either a fast ($v > 60$ km s$^{-1}$), dissociative J-type shock (Neufeld & Dalgarno 1989) or a slower UV-irradiated C-type shock ($v \sim 20-30$ km s$^{-1}$, Wardle 1999). Standard C-type shocks underproduce the observed column density ratio by one order of magnitude or more (Kristensen et al., in prep.). It is not possible to distinguish between the two types of shocks with the current data and availability of model results.

5. Conclusions

The OH lines at 1837.8 GHz from W3 IRS 5 detected with HIFI consist of two components: a broad component, where the triplet components are blended because of the large ionization rate, and a narrow component with velocity resolved hyperfine structure on top. These results indicate that OH emission observed at a lower spectral resolution, e.g. with PACS, can be a blend of envelope and outflow contributions. Low-mass sources reach lower temperatures than the high-mass counterparts at the projected distance of the Herschel beam. From RATRAM models of low-mass sources we thus find a lower excitation, resulting in a weaker envelope contribution to the OH 1837 GHz lines than from W3 IRS 5, consistent with the results for HH 46 in Wampfler et al. (2010). Because the broad component also appears in the line profiles of other species from W3 IRS 5, in particular those of CO and H$_2$O, the outflow is the most likely origin of the emission. Comparison with H$_2$O yields a lower limit on the OH/H$_2$O abundance ratio of 0.028, consistent with an origin from a fast J-type shock or a slower UV-irradiated C-type shock. The narrow emission agrees well with spherical envelope models with a constant OH abundance of $x_{\text{OH}} \approx 8 \times 10^{-9}$. Comparison with new H$_2$O results based on Chavarría et al. (2010) give OH/H$_2$O $\approx 1$ for $T < 100$ K and OH/H$_2$O $\approx 10^{-3}$ at $T \gtrsim 100$ K, consistent with the current picture of the dense cloud chemistry with freeze-out.

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Table A.1. Gaussian fit results to the OH line components using the velocity range [-100, 30] and first order baselines.

| Component        | $T_{\text{lab}}$ [K km s$^{-1}$] | $T_{\text{peak}}$ [K] | $\Delta v$ [km s$^{-1}$] | $v - v_{\text{lsr}}$ [km s$^{-1}$] |
|------------------|----------------------------------|------------------------|---------------------------|-----------------------------------|
| Envelope 1+ → 1- | 3.9 ± 0.4                        | 0.8                    | 4.5                        | 11.9 ± 0.2                        |
| Envelope 2+ → 1- | 11.7 ± 0.6                       | 2.4                    | 4.5                        | 0.8 ± 0.1                         |
| Envelope 1+ → 0- | 5.7 ± 0.5                        | 1.2                    | 4.5                        | -3.3 ± 0.2                        |
| Outflow (blended)| 36.7 ± 1.3                       | 1.3                    | 27.4 ± 1.0                 | -4.1 ± 0.4                        |

Notes. The $v - v_{\text{lsr}}$ velocity scale is given relative to the laboratory frequency of the 2+ → 1− component ($v_{\text{lsr}} = -38.4$ km s$^{-1}$ = 1837.817 GHz).

Appendix A: Gaussian fitting

Appendix B: Line width comparison

The comparison of OH and H$_2$O column densities in the outflow is based on the assumption that the emission arises from the same gas. Figure B.1 illustrates the similar widths of the broad components of OH ($\Delta v \approx 27$ km s$^{-1}$), CO ($\Delta v \approx 29$ km s$^{-1}$), and H$_2$O ($\Delta v \approx 26$ km s$^{-1}$). The broad component of OH is a blend of three hyperfine components with individual widths of $\Delta v \approx 22$ km s$^{-1}$, derived from the best fit slab model (Sect. 3.1).

Appendix C: Slab modeling details

The modeling of the OH line spectrum (cf. Sect. 3.1) is carried out with the slab model code presented in Appendix B of Bruderer et al. (2010). Both OH line components (narrow/envelope and broad/outflow) are represented by a slab in front of a continuum source. The continuum temperature $T_{\text{cont}}$ is derived from the observed single-sideband continuum value and the source is assumed to be fully covered by both slabs. No geometry is included, except that the outflow slab is placed in front of the envelope slab. Each slab has four free parameters per line: the OH column density $N_{\text{OH}}$, the excitation temperature $T_{\text{ex}}$, the line width $\Delta v$, and the position (in velocity space) of the line center $v_{\text{lsr}}$, but the excitation temperature is assumed to be the same for all hyperfine transitions. The normalized level populations of the upper (x$_u$) and lower level (x$_l$) are therefore determined by the Boltzmann distribution at $T_{\text{ex}}$,

$$\frac{x_u}{x_l} = \frac{g_u}{g_l} \exp \left( -\frac{h \nu_0}{k B T_{\text{ex}}} \right)$$

with the statistical weights $g_u$ and $g_l$ of the upper and lower level, respectively, Boltzmann’s constant $k$, Planck’s constant $h$, and the frequency $\nu_0$ of the transition. The radiation temperature $T(\nu)$ is derived from the solution of the radiative transfer equation, using the Rayleigh-Jeans approximation, as

$$T(\nu) = T_{\text{cont}}(\nu) \exp \left( -\tau_{\text{env}} \right) \exp \left( -\tau_{\text{off}} \right)$$

$$+ \frac{c^2}{2 \nu_0 k B} B_{\nu_0} \left( T_{\text{ex}}^{\text{env}} \right) \left[ 1 - \exp \left( -\tau_{\text{off}} \right) \right]$$

$$+ \frac{c^2}{2 \nu_0 k B} B_{\nu_0} \left( T_{\text{ex}}^{\text{env}} \right) \exp \left( -\tau_{\text{env}} \right) \left[ 1 - \exp \left( -\tau_{\text{off}} \right) \right]$$

with $c$ being the speed of light, $B_{\nu_0}$ the Planck function, $\tau_{\text{env}}$ the optical depth of the envelope layer, and $\tau_{\text{off}}$ the optical depth of the outflow layer. The line optical depth of every slab is the sum of the contributions of all $M$ hyperfine components and can be calculated from

$$\tau(\nu) = N_{\text{OH}} \sum_{j=1}^{M} \frac{A_{ul}}{8 \pi (\nu_j^2 - \nu^2)} \left( x_j^{\text{lab}} \frac{g_u}{g_l} - x_j^{\text{lab}} \right) \varphi(\nu)$$

where $A_{ul}$ is the Einstein coefficient and $\varphi(\nu)$ the normalized line profile function of the transition, assumed to be a Gaussian of width $\Delta \nu$ centered at $v_{\text{lsr}}$. This approach takes line overlap into account.

Fig. C.1. 1σ and 2σ contours for the fit of the narrow (envelope) component with slab models. The best fit is indicated by the red dot.