Wideband Beamforming with Rainbow Beam Training using Reconfigurable True-Time-Delay Arrays for Millimeter-Wave Wireless

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Abstract—The decadal research in integrated true-time-delay arrays have seen organic growth enabling realization of wideband beamformers for large arrays with wide aperture widths. This article introduces highly reconfigurable delay elements implementable at analog or digital baseband that enables multiple Spatial Signal Processing (SSP) functions including wideband beamforming, wideband interference cancellation, and fast beam training. Details of the beam-training algorithm, system design considerations, system architecture and circuits with large delay range-to-resolution ratios are presented leveraging integrated delay compensation techniques. The article lays out the framework for true-time-delay based arrays in next-generation network infrastructure supporting 3D beam training in planar arrays, low latency massive multiple access, and emerging wireless communications standards.

Index Terms—True-time-delay array, array architecture, beam training, millimeter-wave communication, wideband systems

I. INTRODUCTION

WIRELESS networks have fueled socio-economic growth worldwide and are expected to further advance to enable new applications such as autonomous vehicles, virtual and augmented reality, and smart cities. Due to shortage of sub-6 GHz spectrum, millimeter-wave (mmW) frequencies play an important role in the fifth generation (5G) communication networks. Recent research and development of 5G mmW networks has revealed that the propagation loss in the mmW band needs to be compensated by antenna array gain and densification of base stations with cell radius as small as a hundred meters. To make radio chipsets power and cost-efficient, state of the art (SOTA) 5G mmW transceivers are designed with phased antenna array (PAA) based subarray architecture. As a consequence, signal processing techniques and network protocols for 5G mmW networks are designed under constraints of PAA architectures.

Future generations of mmW networks will operate in the upper mmW frequency band where more than 10 GHz bandwidth can be used to meet the ever-increasing demands. Their realization will demand addressing a completely new set of challenges including wider bandwidths, larger antenna array size, and higher cell density at the physical infrastructure level as highlighted in Fig. 1. These new system requirements demand fundamental rethinking of radio architectures, signal processing and networking protocols. Major breakthroughs are thus required in radio front-end architectures to enable wideband mmW networks, as most commonly adopted PAA based radios face many challenges in meeting the demanding requirements for different SSP functions.

A large portion of PAA implementations approximate the inter-element delay between the received signals with a phase-shift and hence the spatial processing is performed based...
on the phase difference between the received signals. This approximation simplifies the physical integrated circuit implementation, as compensating a phase shift is much simpler than a time delay. However, this simplification and approximation comes at the cost of limited operating fractional bandwidth of the receiver and will be analyzed further in Section II.

This article brings forward advances in true-time-delay (TTD) arrays that have the potential to significantly impact SSP for emerging wireless communication standards. We use TTD-based PAA [11]–[25] to first establish a contrast with the current phase shift only PAAs [27]–[45] that will be used for both data communications and direction finding. The application of TTD-based PAAs for different SSP functions will have ramifications for future mmW network infrastructure and emerging wireless standards. We next develop a TTD-based PAA exploiting the so-called beam squint phenomenon to achieve precision direction finding overcoming fundamental latency bottlenecks in earlier beam training methods.

II. EXPLOITING DELAY COMPENSATION IN SPATIAL SIGNAL PROCESSORS

PAA operating over a very wide frequency band exhibits frequency-dependent beam pattern in an uncontrollable manner and it often degrades beamforming gain and directionality of the beam. This phenomenon is referred to as spatial wideband effect [46] or beam squint [47]–[49], that becomes more significant in large antenna arrays.

This section will describe recent advances in SSP algorithms and architectures leveraging delay compensating circuits to overcome fundamental limits in analog PAAs. Interested readers are referred to [50] for a similar analysis for hybrid TTD PAAs. We will describe application of TTD arrays to realize different SSP modes when the array is used for data communications or for direction finding. In the former SSP mode, the TTD array will alleviate beam squint effects while in the latter mode, intentional beam squint is introduced to achieve accurate but fast beam-training significantly reducing the search latency in existing analog PAAs. To realize these different SSP modes in a TTD PAA, it is important to understand the trade-offs between the delay range, delay resolution, and modulated bandwidth as shown in Fig. 2. Higher delay resolutions and moderate bandwidth are needed for beam-nulling (independent interference cancellation [51]) whereas large delay range, moderate resolution, and large bandwidths are needed for beam-training. The SSP mode for independent interference cancellation is a corollary of the beamforming SSP and thus will not be studied in this article.

A. Mitigating beam-squint for data communications mode

To alleviate the beam squint effect, the PAA is required to compensate inter-element signal delays before any SSP is done as illustrated in Fig. 3. Assuming a half-wavelength antenna spacing, the delay difference between the received signals in two consecutive antennas \( \Delta T = d \sin(\theta)/c \), which can be also expressed as a frequency-dependent phase shift difference \( \Delta \Phi \) in the frequency domain through the following expression:

\[
\Delta \Phi = 2\pi f \Delta T = \pi \sin(\theta) \frac{f}{f_c} \tag{1}
\]

where \( f \) is frequency. If the signal of interest is narrowband, i.e., \( f/f_c \approx 1 \), the required TTD element can be replaced with a frequency-flat phase shifter (PS). This approximation is the basis of large portion of the SOTA SSP systems [19], [27]–[45]. A generalized implementation of phase shifting based SSP unit is shown in Fig. 4.

As for any approximation, replacing a TTD element with a PS imposes performance limitations. These limitations can be described both in the angular domain and the frequency domain. In the angular domain, PS-based implementation causes the intended angle-of-arrival (AoA) to be frequency-dependent. To be more specific, the intended AoA, for both beamforming and beam-nulling cases, varies with the signal of interest frequency as in:

\[
\theta = \sin^{-1} \left( \frac{f_c \Delta \Phi}{f \pi} \right) \tag{2}
\]

At the center frequency of the band, the PS-based and the TTD-based AoAs are the same and the beam is formed/nullled. As the frequency moves away from the center, the approximation of TTD with a PS becomes less valid and there will be an error between the actual and real intended AoA. This error can be formulated as follows:

\[
\Delta \theta = \left| \sin^{-1} \left( \frac{f_c \Delta \Phi}{f \pi} \right) - \sin^{-1} \left( \frac{\Delta \Phi}{\pi} \right) \right| \tag{3}
\]
This error depends on the actual AoA and the relative frequency of the interest. The maximum error happens at the edges of the frequency band, as the frequency deviates the most from the center frequency. As the error is inversely proportional to the frequency, at the lower side of the frequency band error will be larger than the higher side of the band and this maximum error can be found as:

\[
\Delta \theta_{\text{max}} = \left| \sin^{-1} \left( \frac{f_c - \Delta \Phi / 2}{f_c - \text{BW}/2} \right) - \sin^{-1} \left( \frac{\Delta \Phi}{\pi} \right) \right|
\]  

(4)

where BW is the signal bandwidth and BW/f c is called the fractional bandwidth. In Fig. 5 the maximum error in the angular domain for a PS-based SSP unit is plotted versus the ideal intended AoA, for three cases of fractional bandwidths. In this plot the AoA range is limited to ±60°, since for larger AoAs the actual AoA can be as high as ±90° and the error in those cases does not reflect the severity of the PS-based implementation. As it can be seen, this error can get as high as 22° which results in non-alignment with the intended transmitter and consequently loss in the desired signal (beamforming case) or imperfect cancellation (beam-nulling case). The frequency-dependent approximation of a TTD element with a PS results in frequency-dependent beamforming gain that acts as a bandpass filter [20], [22], and imperfect frequency-dependent beam-nulling that results in wideband interference leakage [23], [51].

The beamforming gain in a PS-based N-element receiver can be modeled as the absolute value of the inner product \( G(f) = |w^H a| \), where w is a receive beamformer and a is a spatial response vector. Assuming a phase difference of \( \Delta \phi \) between neighboring PSs, the n-th element of w is defined as \( [w]_n = \exp(-j(n-1)\Delta \phi) \). On the other hand, using (1), the n-th element of a is defined as \( [a]_n = \exp(-j(n-1)\Delta \Phi) \). Expressed as a sum of complex exponentials, the gain \( G(f) \) becomes

\[
G(f) = \left| \sum_{n=1}^{N} e^{j(n-1)(\Delta \Phi - \Delta \Phi)} \right| .
\]

(5)

In Fig. 6 the normalized beamforming gain \( G(f)/N \) for intended AoA of 45° versus normalized frequency \( f/f_c \) of the input signal for cases of \( N = 4, 16, 64 \), are plotted. The beamforming gain in a PS-based implementation acts as bandpass filter for the desired signal. Similar to a filter, the 3-dB fractional bandwidth (FBW_{3dB}) can be defined as the fractional bandwidth where the beamforming gain drops 3 dB compared to the maximum value (N). As proven in [52], [53], for large values of N, the FBW_{3dB} is given as:

\[
\text{FBW}_{3\text{dB}} \approx \frac{1.772}{N|\sin(\theta)|^2}
\]

(6)

For larger arrays FBW_{3dB} becomes smaller and the approximation of a TTD element with a PS becomes less valid. Similar to the outcome of the beam squinting error, as the intended AoA increases, the FBW_{3dB} gets smaller and the effective error increases.

B. Beam-squint array for beam-training mode

Beam-training is a part of initial access (IA) protocol in mmW networks that achieve alignment of beamforming directions to realize a maximum gain between base station (BS) and user equipment (UE) [54], [55]. Beam-training using PAA requires extensive beam sweeping to estimate angle-of-departure (AoD) and AoA (Figure 7(a)), as it can only probe one steering direction at a time. As a result, PAA-based IA latency increases with array size and number of users [54]. The majority of existing mmW beam-training algorithms was designed for analog PAA due to their power efficiency. Phased arrays use frequency-flat PS in all antenna branches to steer/combine the signal in a desired direction. With a single mmW chain, PAAs can synthesize only one spatial beam with all frequency components being aligned in the same direction. The existing beam-training schemes with PAAs include various types of exhaustive beam sweeping where different beam candidates are sequentially used for channel probing to find the AoA [56], [59]. The required number of probing beams
linearly scales with the number of antenna elements $N$, thus, the beam-training overhead becomes a bottleneck for low-latency communications. SOTA IA approaches based on 5G requirements are limited to narrowband pilots and relatively small number of antennas, so the IA latency is acceptable. However, future evolutions of mmW-nets will be IA latency limited and would require using wideband pilots and new radio architectures that can probe a large number of AoA/AoD in parallel as illustrated in Figure 1(b).

To address this fundamental issue in mmW PAAs, this article will introduce a fast beam training method leveraging TTD arrays. Instead of suppressing the beam squint effect evident in mmW arrays, we will exploit this effect to our advantage by introducing intentionally large time delays in each antenna branch to realize frequency-dependent probing beams which can be exploited to accelerate the channel probing capability. These frequency-dependent beams will be fully controlled by adjusting the delay introduced in TTD circuits [60].

In summary, this article presents reconfigurable delay compensating circuits with large delay range and bandwidth, and finer delay resolution to realize wideband mmW SSP. Section III summarizes the TTD SSP architectures highlighting the challenges associated with realizing large delay compensation with fine resolution at different domains in the receiver chain. Section IV discusses the fast beam-training algorithm and practical design considerations for analog PAAs leveraging TTD SSP architecture. Section V will present the hardware implementation of reconfigurable time delay units enabling different SSP modes along with hardware validation methods for wideband PAAs. Section VI presents future works expanding the proposed TTD-based PAAs for beam-training with planar arrays, multiple access applications, and standardization of wireless protocols. Section VII concludes this article.

III. OVERVIEW OF MMW TTD PAAS

This section describes the possible architectural choices for TTD PAAs. The design of PAAs are based on two principles: (1) phase/delay alignment of signals either in transmit or receive path, and (2) summation of phase/delay aligned signals. To align the received signals in a PAA, delay elements should provide the proper delay to each received signal. The delay can be applied to the signal in mmW, LO, baseband, or digital domains. When the fractional bandwidth of the signal or the required delay range in the phased array system is small, the delay is approximated by a phase shift as discussed before. There are different topologies that are common in the implementation of PAA transceivers (Fig. 8) such as radio frequency (RF) phase shifting [61]–[64], LO phase shifting [65], baseband (BB) phase shifting [67], [68], and digital phase shifting [69]. In the RF phase-shifting architecture, after applying the required phase shift in each RF path, the signals can be combined together. LO phase shifting architecture uses the PS in the LO port of the mixer. In BB and digital phase-shifting architecture, the received signals are aligned after downconversion, using analog circuitry in baseband or in a digital processor. Either of these architectures is a good candidate when the signal’s fractional bandwidth is small, or the required delay range in the PAA is small.

For large delay-bandwidth product cases, delay units are necessary to prevent beam squint. Similar to a PS-based PAAs, the location of the time delay unit makes possible multiple architectures (mmW/RF path, LO port of the mixer, BB, or digital domains). In the mmW/RF TTD architecture, the time delay unit is placed in the mmW/RF domain before the downconversion. The received signals at each receiver path can be combined constructively, as shown in Fig. 8(a). The mixer is shared between multiple paths and only one LO signal is necessary which allows significant area and power reduction. As the signals are combined before downconversion, interferers are removed due to spatial filtering, which reduces the linearity requirements of the blocks after the combiner. Although there are different implementations of the
mmW/RF TTD-based PAAs, these implementations occupy a large area on the chip and there are serious limitations on the delay range. Table II highlights the integrated mmW/RF TTD implementations over the past decade starting with the seminal work by Chu and Hashemi in 2007. Placing the TTD element in the LO path of the mixer does not resolve these limitations especially when handling wideband range. Digital TTD PAA is the same as a digital phased array and the challenges are the same such as high power consumption including the need for highly linear analog-to-digital converter (ADC) as well as other linear elements. However, there are promising TTD-based PAAs in BB with large delay-bandwidth products [22], [70]. Table II highlights recent SOTA TTD-based PAAs and delay lines implemented at BB.

In an array with BB TTD elements as shown in Fig. 9(a) [22], instead of delaying the down-converted and phase shifted signals from the antennas followed by sampling and digitization, the signals are sampled at different time instants. Thus, the complexity of delaying signals is shifted to the clock path where precise and calibrated delays can be applied in the advanced semiconductor technology nodes. More importantly, a large delay range-to-resolution ratio can be easily realized while supporting a relatively larger number of antennas and bandwidth. The switched-capacitor adder based implementation requires multiple time-interleaved and delay compensated phases for formation of the beam [22]. In the sampling phase, the input signal from each channel is first sampled (with delayed time-interleaved clocks) on a sampling capacitor. After the last sampling phase, the stored charges on each capacitor corresponding to each channel (and each time-interleaved phase) are summed to form the beam. However, since time delay in BB is not mathematically equivalent to time delay in the RF domain, a small phase shift is still needed, it can be implemented in the BB with a time delay equal to \( \tau_d \) plus a phase shift equal to \( -\omega_L \tau_d \) [20], [22], [37]. The BB TTD architecture shown in Fig. 9 is hereby referred as discrete-time TTD SSP.

A PS can be implemented in the RF, LO, BB, or digital domain to provide the required phase shift to the BB time delay units. The mmW/RF PS can be limited by the maximum delay-bandwidth product of the receiver. Digital implementation of the TTD or PS is similar to digital phase-shifting architecture with each RF path requiring an ADC implementation of the TTD or PS is similar to digital phase-shifting architecture with each RF path requiring an ADC which increases the power consumption of the whole system considerably. ADCs should be linear enough to tolerate the large interferences which further increases the whole system’s power consumption. Placing a PS in BB or LO is another feasible option (Fig. 9). In these architectures, each RF path has a dedicated mixer and an LO signal. PS in the LO port of the mixer should operate at the LO frequency. However,
the PS in the BB or intermediate frequencies has to operate at lower frequencies. Though the loss and phase error of the PS in RF frequencies is higher than the PS at BB, the PS at the BB has to operate at a much higher fractional bandwidth while the PS in LO path only deals with a single tone signal (Fig. 9a). The PS can be implemented in the LO [71] as well as conventional PS architectures.

BB PS using vector summation is also another option. Vector summing PS is based on the weighted summation of quadrature signals. Quadrature signal generation is possible using a quadrature coupler, polyphase filters, or using quadrature mixers. Quadrature couplers at the BB occupies a large chip area and thus less preferred. Polyphase filters usually are narrow-band which contradicts with the large-delay bandwidth required. The use of quadrature downconversion mixers is another option though at the expense of routing complexities.

The next section presents the framework of leveraging discrete-time TTD SSP for fast beam-training followed by details on hardware implementation and experimental validation of TTD SSP.

IV. Rainbow Beam-Training Using Discrete-Time TTD SSP

This section describes the design of TTD array parameters, which enable a training codebook of frequency-dependent beams to be synthesized. We also explain the corresponding frequency-domain digital signal processing (DSP) algorithm [60]. We further discuss the practical aspects of TTD beam training including the sensitivity to hardware impairments, power allocation and the peak-to-average power ratio (PAPR) problem in orthogonal frequency-division multiplexing (OFDM) systems, and achievable beam training distance.

A. Introduction to Rainbow beam-training for mmW PAs

Recent work on mmW and sub-THz beam-training has been focused on minimizing the required overhead using frequency-dependent beam steering/combining [13], [50], [60], [72]–[74]. The main idea is to leverage different antenna architectures that can synthesize rainbow beams to probe the entire angular range simultaneously. Each rainbow beam is associated with a different frequency, thus, information of the best steering/combining direction is embedded in the signal spectrum and it can be obtained through simple frequency-domain DSP. In [72], the authors proposed to use leaky wave antenna (LWA) for a single-shot AoA estimation. In [73], a delay-phase array architecture was proposed for fast beam tracking with rainbow beams at THz frequencies. TTD array architectures in [13] implemented delay elements in RF, which are known to suffer from low scalability in terms of required area and power efficiency when the array size becomes large. In our recent work in [50], [60], [74], we proposed a scalable TTD arrays with delay elements implemented in baseband for a single-symbol mmW beam training in an OFDM system. The key idea was to exploit signal delaying in each antenna branch to exacerbate the wideband spatial effect (beam squint) among subcarriers in a controllable manner, i.e., to create a frequency-dependent codebook which probes all angular directions at once. This is achieved by properly configuring the delay and phase taps in a TTD array.

B. TTD codebook and DSP algorithm design

In our recent work we introduced TTD-based beam-training at the UE side that requires only one OFDM symbol [50], [60]. We assume that the BS with N_R antennas uses a fixed frequency-flat precoder v ∈ C^{N_T} designed according to the previously estimated AoD. The received signal Y[m] at the m-th OFDM subcarrier can be expressed as follows

\[ Y[m] = w^H[m]H[m]vs[m] + w^H[m]n[m], \]

where w[m] ∈ C^{N_R} is a frequency-dependent UE TTD combiner, H[m] ∈ C^{N_T x N_R} is a channel matrix, s[m] is a pilot, and n[m] ∼ CN(0, σ_n^2I_R) is a noise vector at the m-th subcarrier, respectively. The n-th element of w is defined as

\[ |w[m]|_n = \alpha_n \exp\left(-j(2\pi(f_m - f_c)\tau_n + \phi_n)\right), \]

where \( \alpha_n = 1 \), \( \tau_n \), and \( \phi_n \) are the gain, delay tap, and phase tap in the n-th antenna branch, respectively.

Assuming the bandwidth BW and a uniform linear array (ULA) with a frequency-flat spatial response at the UE side, it was shown in [60] that a codebook of rainbow beams which cover the entire angular range \([-\pi/2, \pi/2]\) can be created by setting the delay taps \( \tau_n \), \( \forall n \), as follows

\[ \tau_n = (n - 1)\Delta \tau, \forall n, \text{ where } \Delta \tau = 1/BW, \]

Since the taps in [9] are proportional to the Nyquist sampling period, the codebook can be obtained without the need to implement a fractional ADC sampling. In such a codebook, the rainbow beam associated with the subcarrier frequency \( f_m \) is pointing in the angle \( \theta_m \) given as follows [60]

\[ \theta_m = \sin^{-1}\left(\mod(2f_m\Delta \tau + 1, 2) - 1\right). \]

An example of the resulting TTD codebook for a UE with \( N_R = 16 \) antenna elements is provided in Fig. 10. To probe \( D = N_R = 16 \) directions, \( M = 16 \) subcarriers need to be used. The codebook can be designed to be more robust in frequency-selective channels by mapping \( R \) different subcarriers to each probed direction. This is achieved by increasing the delay difference between antenna elements \( R \) times, i.e., \( \Delta \tau = R/BW \) [74]. With \( R \) being the codebook diversity order

![Diagram](image-url)
The pointing angles $\theta_n$, $\forall m$, of rainbow beams can be jointly rotated by using the frequency-flat PSs in the TTD array. A rotation of $\theta_{\text{rot}}$ requires the phase taps $\phi_n$, $\forall n$, to be set as follows

$$\phi_n = (n-1)\Delta \phi, \forall n, \text{ where } \Delta \phi = \pi \sin(\theta_{\text{rot}}). \quad (11)$$

The rotated angles can then be expressed as $\theta'_m = \theta_m + \theta_{\text{rot}}, \forall m$.

With this codebook and described frequency-to-angle mapping, the information of the dominant propagation angle can be acquired with simple frequency-domain DSP. Given the received signal in (7), a coarse AoA estimate $\hat{\theta}$ is given as $\hat{\theta} = \theta'_{m^*}$, where the angle $\theta'_{m^*}$ corresponds to the subcarrier with the strongest received signal power. Mathematically, the estimation can be expressed as

$$\hat{\theta} = \theta'_{m^*}, \text{ where } m^* = \arg\max_m |Y[m]|^2. \quad (12)$$

If the codebook diversity is $R$, the power $|Y[m]|^2$ is averaged across all $R$ subcarriers $m$ mapped into the same direction before angle estimation.

The estimation accuracy can be improved by designing a high-resolution dictionary-based algorithm that relies on the codebook with diversity order $R$ [74]. The average received signal power in all probed directions can be correlated with the transmit signal power to be allocated to a lower number of subcarriers.

C. Practical considerations in TTD beam-training

1) Sensitivity to hardware impairments: In practice, errors in different hardware components can distort the delay taps in (9) and phase taps in (11) and thus affect the designed beam training codebook. We assume that delay errors can be modeled as Gaussian random variables, such that the distorted taps are $\tilde{\tau}_n \sim N(\tau_n, \sigma^2_\tau)$, where $\sigma^2_\tau$ is the error variance. The phase errors occur due to imperfect PSs, LOs, imbalance between in-phase and quadrature-phase samples, or other hardware errors. Similarly as with the delays, we model the distorted phase taps as $\tilde{\phi}_n \sim N(\phi_n, \sigma^2_\phi)$, where $\sigma^2_\phi$ is the error variance. In addition to the phase and delay errors, we consider distorted gain $\hat{\alpha}_n$ in all antennas branches. The gains are modeled with a log-normal distribution, i.e., $10 \log_{10}(\hat{\alpha}_n) \sim N(0, \sigma^2_\lambda), \forall n$.

and $D$ the number of probed directions, TTD beam training requires a waveform with $M = DR$ loaded subcarriers.

The assumed parameters for numerical evaluation are shown in Table III. The average received signal power in all probed directions can be correlated with the transmit signal power to be allocated to a lower number of subcarriers. The curves with gain error (dashed with stars) and phase error (dashed with diamonds) are associated with the lower and upper x-axis, respectively.

![Fig. 11. Impact of gain and phase errors on performance of two TTD beam training algorithms [74]. The curves with gain error (dashed with stars) and phase error (dashed with diamonds) are associated with the lower and upper x-axis, respectively.](image)

![Fig. 12. Impact of delay error on performance of two TTD beam training algorithms [74].](image)
Fig. 13. Illustration of OFDM power allocation in (a) conventional beam training and (b) TTD beam training.

Fig. 14. PAPR comparison between proposed and fully loaded OFDM waveforms, assuming BPSK or QPSK symbols.

The signal power in the proposed OFDM waveform is divided among $M$ subcarriers, the SNR per subcarrier is given by the following expression:

$$\text{SNR}_{\text{per}} = \frac{G_T G_R \lambda^2}{(4\pi d)^2} \frac{P_T}{\Delta B W N_0 M},$$

(13)

assuming a free-space path loss model. The terms $G_T = 20 \log_{10} (N_T)$, $G_R = 20 \log_{10} (N_R)$, $\lambda$, and $d$ represent the transmit beamforming gain, receive beamforming gain, wavelength, and distance between the BS and UE. Power spectral density of the noise is denoted as $N_0$, while $\Delta B W = B W / (M_{\text{tot}} - 1)$ represents the subcarrier spacing. Note that the SNR per subcarrier is $M_{\text{tot}}/M$ times larger than with a fully loaded OFDM waveform. Since the proposed DSP algorithm considers only $M$ loaded subcarriers with high SNR, angle estimation in (12) is not noise-limited. Further, due to a lower number of used subcarriers, the proposed OFDM waveform for TTD beam training results in a more than 2dB lower PAPR than a fully loaded OFDM waveform, as presented in Fig. 14 where we assumed the same simulation parameters as in the previous subsection. We used a cyclic prefix of 128 samples and assumed that subcarriers are loaded either with binary phase shift keying (BPSK) or quadrature phase shift keying (QPSK) symbols.

Although the proposed frequency-dependent beam-training can benefit from a higher SNR per subcarrier, the supported distances between the BS and UE are reduced compared to the PAA beam sweeping approach. This is because the UE has a lower total received signal power. Specifically, with the codebook in Fig. 10 which probes $D$ different directions, roughly $1/D$ of the signal power is received per direction. The received signal power corresponds to the subcarriers that probe the dominant AoA. To evaluate the impact of lower received signal power on the beam-training performance, we compared the AoA RMSE of TTD-based algorithms and PAA-based beam sweeping at different distances between the BS and UE. We assumed a non-line-of-sight scenario and modeled the path loss according to mmMAGIC channel [75]. We considered two array sizes at the UE, including $N_R = 16$ and $N_R = 32$. With $N_R = 16$, $D = 32$ directions are probed, while with $N_R = 32$, $D = 64$ directions are probed. Other parameters are the same as in the previous subsection. The comparison results are presented in Fig. 15. PAA-based beam sweeping combines the entire signal bandwidth in each probed direction and thus achieves a high received signal power and reliable angle estimation at different distances. Nevertheless, it requires large overheads of 32 and 64 OFDM symbols to do so when $N_R = 16$ and $N_R = 32$, respectively. On the other hand, TTD beam training algorithms are based on a single OFDM symbol and their performance is comparable to that of exhaustive PAA beam sweeping. However, supported distances in TTD beam-training are reduced, assuming that the signal cannot be detected when its total post-combining power falls below post-combining noise level. In our simulations, this happens at $d = 170m$ for $N_R = 16$ and $d = 150m$ for $N_R = 32$, as highlighted in Fig. 15. We note that with a more sophisticated detection algorithm that exploits the waveform structure, beam training capabilities and supported distances of TTD arrays could increase. We leave a more detailed theoretical study of supported distances and better detection algorithms for future work.

V. RECONFIGURABLE DISCRETE-TIME TTD SSP HARDWARE DESIGN CONSIDERATIONS

In this section, we describe the design and hardware implementation of reconfigurable time delay units in the discrete-time TTD SSP shown in Fig. 2 applied to both the data communications as well as beam-training SSP modes.

A. Important sub-systems in discrete-time TTD SSP

The analog array though more energy efficient when compared to hybrid TTD and digital arrays [50] require larger unity-gain bandwidth amplifiers to have similar performance. The circuit performance is further constrained with the parasitic capacitance, routing losses, crosstalk, and any possible
mismatches during fabrication evident at multiple levels including silicon, packaging, or printed circuit board. Design considerations for the key blocks are described here to ensure low-power consumption is upheld for analog arrays as compared to hybrid or digital TTD SSP [50] including its ability to achieve fractional delays with high precision. This section presents design considerations for the key design blocks: (i) sample-and-hold, (ii) wideband signal combiners, and (iii) precision clock generation. Fig. 16 shows a more detailed illustration of the discrete-time TTD SSP. Interested readers can refer to [22], [26], [50], [51] for further understanding.

1) Sample-and-hold: The design constraints for the input sample-and-hold draws parallel to the design requirements of a high-speed time-interleaved ADC [76]. Different interleaver configurations can be analyzed based on a simplified switch model in which the switch resistance and capacitance are linked to the technology. To reduce effect of sampling jitter, it is preferable to sample first followed by subsampling however at the cost of additional source followers which can significantly impact power consumption and linearity. To relax the power consumption, the first sampler can be interleaved (typically by 2 or 4) at the cost of slightly higher mismatch and jitter [77].

2) Signal combiners: The signal combiner is a critical component for wideband discrete-time beamforming that requires careful design considerations of several parameters including gain, bandwidth, number of summing channels (each channel refers to a downconverted RF signal from each antenna element), dynamic range, and power consumption. The multi-parameter optimization considering the required design specifications for each system can be addressed using either a closed-loop or open-loop summing amplifiers, shown in Fig. 17(a). In [22], a closed-loop operational transconductance amplifier (OTA) is used whose design complexity and power consumption are scaled exponentially with the bandwidth. To support larger bandwidths and higher number of antennas, a closed loop integrator using ring amplifier [78], [79] was demonstrated in [26]. Ring amplifiers are technology scalable lending them good candidates to beamform signals from even larger number of antenna elements. In contrast to closed-loop amplifiers, summing can also be performed through daisy-chain linked voltage-to-time converter (VTC)s as shown in Fig. 17(b). The serialized VTCs each acting in open-loop is digitized by a multi-bit time-to-digital converter (TDC) creating an equivalent of matrix-multiplying ADC.

3) Precision clock generation: The required sampling phases of the discrete-time SSP can be generated on-chip as illustrated in [22], [26]. To achieve higher precision and matching following Nyquist criterion as well as use the same architecture for different SSP modes, the clock generation requires N low-power precision phase interpolator (PI) and time-interleavers [22], [50], [51]. The time-interleaver output is applied to interleaved multiply-and-accumulate units that enables them to span the required delay range while meeting the Nyquist bandwidth.

High precision linear PSs are desired to meet the delay range and resolution requirements for the switched-capacitor array as discussed in Section III. Recent works have demonstrated PSs as digital-to-phase generator in different applications including clock-and-data recovery [80], [81] and outphasing transmitters [82], [83]. In general, several architectures have been proposed to implement PI which generates output of phases of weighted sum of two input clock phases based on the digital input code.

The underlying concept of PI can be studied from [84] which describes the process as addition of two phase-shifted edges to produce a new edge with the transition in between them. The output is a superposition of two exponential curves formed by the merged driver output resistance and the capacitive load. The linearity of the PI not only depends on the time difference between the input signals but also their rise times. It has been observed that the non-linearity for a step input response is more whereas it is less for the inputs with finite rise time inputs.

The current-steering digital-to-analog converter (DAC) have been popular architectures for implementing PI [85]. However,
the linearity and resolution are greatly impacted by the DAC. As mentioned above, to generate finite rise time at the input, a slew rate control buffer is implemented which requires additional power. The summation of the direct in-phase and quadrature-phase however causes nonlinearity with respect to the codes. Alternatively, current-mode logic based PI architectures can be adopted if the inputs are sinusoidal signals. Instead of interpolating between two consecutive quadrature phases, it can be done in multiple cascaded stages. Interpolation between signals with small phase differences (< 45°) is more linear than direct interpolation between the quadrature inputs. Though the current-mode logic based PI has lower swing which consumes less dynamic power, it suffers from linearity issue where as the inverter-based PIs suffers from high dynamic power. Additionally, the PI’s output gets affected by the power supply variations. Low-dropout regulators can be applied between the main power supply and the PI supply to alleviate this issue. As such, its important to consider the design trade-offs for N PIs specifically linearity and power consumption.

B. Multi-antenna testbed and validation

Another important step in the design process is developing the test interface between the mmW front-end and the BB TTD SSP as well as the digital back-end. The wide modulated bandwidths and the large number of downconverted channels from mmW to baseband due to both differential and quadrature configurations challenges the signal generation and post-processing. In addition, all the channels should be synchronized in time with picosecond accuracies to enable efficient data communications. Fig. 18 shows a sample closed-loop testbed for 800 MHz TTD SSP recently demonstrated in [26]. High speed DACs and ADCs in ZCU RFSoC family make it possible to generate wideband signals from DACs and perform data capture from the high speed ADC through the same graphic user interface control which serves both as an arbitrary waveform generator and spectrum analyzer in [22]. In [26], 800 MHz modulated bandwidth with 16 synchronized channels was generated and the outputs post-processed after digitization in MATLAB offline.

Besides synchronization and large number of channels, repeated parameterized sweeps across frequencies and angles to characterize a multi-antenna transceiver undertakes significant efforts without closed-loop automation in place. In [23], the TTD SSP (in particular, TDC and the time amplifiers) were optimized using particle swarm optimization techniques from [80]. While the optimization was limited to TDC only and not the entire SSP, this method shows the potential opportunities to further extend the test bench automation for closed-loop signal path optimization.

In their recent work, the authors have used computer vision techniques for testbed automation in [87]. These techniques reduces the strenuous manual calibration and test process significantly and enables generation of data-intensive 3D plots (Fig. 19a) and frequency-angular maps (Fig. 19b) that can be used to create accurate dictionaries for calibration in data communications mode. The shown plots represent 72 individual configurations when the 4-element array is configured to -45° with 500 MHz modulated bandwidth at the input. The measured half-power beamwidth is close to the theoretical estimated 35°. Similar map can be generated for the rainbow beam-training as shown in Fig. 19b which shows the efficacy of the proposed algorithm. Additional measurement details for these plots are captured in [87]. The automated test process further minimizes the human errors in the manual process. In addition, this enables benchmarking entire system from the antenna to the higher network layers combined with machine learning algorithms in future.

VI. FUTURE WORK

A. 3D rainbow beam with planar TTD array

In principle, the frequency dependent beam steering can be extended into the planar TTD array. In our recent work [88] we studied beamforming codebooks with the uniform delay steps $\Delta \tau_x, \Delta \tau_y$, introduced in the antenna elements in the x-y plane before combining, i.e., the received signal in the $(i, j)$-th element is delayed by $(i - 1)\Delta \tau_x + (j - 1)\Delta \tau_y$. We showed that uniform delay spacing can create 3D beams such that different frequency components are steered toward a unique spherical direction $(\theta, \phi)$. Further, the entire 3D angular space can be covered by at least one beam. Fig. 20 presents the frequency dispersing steering for 10 frequency components. However, this preliminary study also reveals a number of design challenges from both circuits and system perspectives. On the one hand, the required maximum delay range is increased. For planar array with a total $N$ elements, the required delay range is at least $2(N - 1)/\text{BW}$, a factor of 2 larger than its linear array counterpart. On the other hand,
Proposed SS block design

C. Compatibility of TTD Beam Training with 5G Standard

Exhaustive beam sweeping with synchronization is the main part of the IA procedure in 5G New Radio Standard. It is performed using periodic bursts of up to 64 SS blocks, each associated with a different steering direction [55]. An SS block is a group of 4 consecutive OFDM symbols with 240 subcarriers (20 resource blocks) that carry the Primary Synchronization Signal (PSS), Secondary Synchronization Signal (SSS), and DeModulation Reference Signal (DMRS). The PSS and SSS are leveraged for synchronization between the BS and UE, while the DMRS can be used to estimate the received power associated with that direction, i.e., SS block.

Since the proposed TTD beam training is fundamentally different from beam sweeping, its compatibility with the current 5G New Radio Standard becomes an important problem. In our preliminary work, we proposed a different design of the SS block, which exploits wide available bandwidth at mmW frequencies and supports TTD beam training, as illustrated in Fig. [21]. In the proposed design, the existing reference signals are repeated multiple times across the operating bandwidth. With such training waveform, the UE is capable of receiving at least one entire legacy SS block using its frequency-dependent beam steering. The UE can then leverage DSP to extract the reference signals to achieve synchronization with the BS and determine the best steering direction. The proposed SS block design removes the need for SS bursts and thus minimizes the required overhead in TTD beam training. However, the design depends on different system parameters, including the number of subcarriers, number of UE antennas, and resolution of UE beam probing. We plan to address these practical design questions in our future work.

VII. Conclusions

Reconfigurable TTD arrays are essential for emerging mmW wireless communications demanding wide bandwidths with ultra-low-latency in direction finding compared to current wireless standards. This magazine article presents a comprehensive overview of the recent developments in TTD arrays enabling multiple SSP functions. Delay compensation techniques are exploited to prevent beam squint during data communications while introducing intentional beam squint for fast beam-training. The article combines the beam-training algorithm with the underlying architectural and circuit design considerations. The exciting developments in TTD arrays presented herein lays out a future path for enabling next-generation network and physical infrastructure wireless solutions on a large-scale with 3D direction finding for communications-on-the-move applications, massive machine type communications, and standardization in emerging wireless standards.

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