Field-sensitive addressing and control of field-insensitive neutral-atom qubits

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The establishment of a scalable scheme for quantum computing with addressable and long-lived qubits would provide a route to harnessing the laws of quantum physics to solve classically intractable problems. The design of many proposed platforms for quantum computing is driven by competing needs: isolating the quantum system from the environment to prevent decoherence, and easily and accurately controlling the system with external fields. For example, neutral-atom optical-lattice architectures provide environmental isolation through the use of states that are robust against fluctuating external fields, yet external fields are essential for qubit addressing. Here, we demonstrate the selection of individual qubits with external fields, while the qubits are in field-insensitive superpositions. We use a spatially inhomogeneous external field to map selected qubits to a different field-insensitive superposition, minimally perturbing unselected qubits, despite the fact that the addressing field is not spatially localized. We show robust single-qubit rotations on neutral-atom qubits located at selected lattice sites. This precise coherent control should be more generally applicable to state transfer and qubit isolation in other architectures using field-insensitive qubits.

The ability to address individual qubits is a vital component of most quantum-computing architectures. In the case of neutral-atom qubits held in an optical-lattice register1,2,3, addressing generally requires the interaction of specific atoms with a control field. Of long-standing concern is the difficulty of addressing only selected atoms amongst an ensemble of ≈ 108 atoms in nominally identical lattice sites. One approach is to use long-period lattices or arrays of independent single-atom traps sufficiently spaced to address with a focused optical beam4,5; in this case, the optical diffraction limit sets a bound on the qubit register spacing (and therefore register density). Alternatively, experiments using the Mott insulator transition in optical lattices result in large arrays of subwavelength-separated single ground-state atoms, which are useful for collisional and exchange quantum gates6,7,8. Schemes similar to magnetic resonance imaging for addressing subwavelength-separated qubits have been proposed and demonstrated, wherein an externally applied gradient field shifts local energies, mapping spectroscopic resolution to spatial resolution9,10,11; however, these schemes require that the qubits be in field-sensitive states, a requirement that is at odds with the need for long coherence times.

Here, we demonstrate how to combine environmental insensitivity and site-specific subwavelength addressability, as illustrated in Fig. 1. Our scheme is based on a register of qubits, each in a superposition of storage states |0⟩ and |1⟩, the energy difference of which is insensitive to external magnetic fields, a significant source of environmental decoherence. (Such pairs of states are known colloquially as ‘clock states’ owing to their utility as frequency standards.) In addition, each qubit has a second pair of clock states, the working states |0′⟩ and |1′⟩, which have a different transition frequency from that of the storage states. Whereas transitions between the storage states (|0⟩ ↔ |1⟩) or between the working states (|0′⟩ ↔ |1′⟩) are insensitive to external fields, the transitions between storage and working states (such as |0⟩ ↔ |0′⟩) are field sensitive. Application of a field gradient thus spectrally selects a qubit from the register, enabling frequency-sensitive (and therefore position-sensitive) mapping of the selected qubit’s coherent superposition between storage states and working states. Once the selected qubit has been transferred to the working states, we can then carry out isolated arbitrary single-qubit operations on the selected qubit alone. Remaining qubits (still in the storage states) are unaffected by both the mapping process and the subsequent control operation on the selected qubit. One can then map the selected qubit back to storage states, resulting in a qubit register with the addressed qubit in a new arbitrary superposition of storage states. This idea may be applicable to other physical systems vulnerable to optical or electrical crosstalk; see, for example, refs 14 and 15, relaxing the required isolation for control fields used to address individual qubits in a spatially dense register.

We demonstrate this scheme in an optical-lattice-based ensemble of registers, where each register is composed of two separately trapped 87Rb atoms acting as qubits A and B. The storage and working states of the qubit are encoded in four hyperfine sublevels of the ground-state manifold of 87Rb, which can be coupled with resonant microwave radiation. Both qubits are initialized in the storage-state superposition α|0⟩ + β|1⟩. After applying a localized effective magnetic field, we spectrally select qubit A and map it into the working-state superposition α′|0⟩′ + β′|1⟩′, where θ is a systematic phase depending on the details of the mapping process. Qubit B remains in the initial storage-state superposition. We then apply a control operation on the working transition, transforming qubit A into the new state α′|0⟩′ + β′|1⟩′. Using a modified Ramsey technique, we verify the basic features of this scheme: namely, that storage-state coherence is unaffected by the application of the field gradient, and that the addressable mapping process is coherent.

Our register confinement is provided by a double-well optical lattice generated by a Ti:sapphire laser operating at 810 nm (see the Methods section and ref. 16). We use the states |F = 1, m_F = −1⟩ and |F = 2, m_F = 1⟩ as storage states |0⟩ and |1⟩, and the states |F = 1, m_F = 0⟩ and |F = 2, m_F = 0⟩ as working states |1⟩′ and |0⟩′. At our operating field near 323μT, the linear
is roughly consistent with the observed dephasing time. We also measure the magnitude of the differential shift as a function of lattice intensity (discussed below). The inhomogeneity of the differential light shift is the main technical limitation on coherence in our ensemble of storage qubits, and can be improved by making the lattice beams more homogeneous and detuning the lattice farther from resonance, as with the $\lambda = 1.06 \mu m$ lattice used for precision spectroscopy in ref. 22. In addition, dynamical decoupling techniques have been shown to be useful in reducing the effects of inhomogeneous broadening23,24. A simple spin–echo pulse sequence, which rephases time-independent inhomogeneous dephasing, gives a residual coherence time $T_2$ in excess of 300 ms, probably limited by drifts in lattice intensity (and thus differential light shift) that cannot be filtered by a single echo. In an analogous measurement, Fig. 2b shows that the working-state coherence exhibits a shorter dephasing time of $T_2' = 21(2) ms$, dominated by background magnetic field gradients.

In contrast to the field-sensitive qubit states, the transitions $|0\rangle \to |0'\rangle$ or $|1\rangle \to |1'\rangle$ are field sensitive. This sensitivity enables spectroscopic qubit addressing, but requires that state transfers be carried out fast enough to avoid the qubits’ vulnerability to field inhomogeneities while they temporarily occupy the field-sensitive superpositions $|0'\rangle + |1'\rangle$ or $|0\rangle + |1\rangle'$ during the transfer from storage states to working states, as in Fig. 1b. We measure this timescale using the standard Ramsey method on the field-sensitive transition $|0\rangle \to |0\rangle'$, giving $T_2' = 500 \mu s$, roughly 100 times shorter than that of the clock states.

To directly determine the impact of this field sensitivity on the mapping from storage to working states, we developed a modified Ramsey sequence that is sensitive to decoherence in the mapping process. This sequence is composed of the standard opening $\pi/2$-pulse on the storage transition, followed by $\pi$-pulses mapping storage states to working states, and closed by a final $\pi/2$-pulse on the working transition. Whereas the standard Ramsey sequence depends only on the relative phase of the two (equal-frequency) $\pi/2$-pulses, our modified sequence requires phase control of four different microwave signals, including the two mapping $\pi$-pulses. As all of our pulses have different frequencies, the meaning and control of the relative phases involved is more subtle.

In particular, each modified Ramsey sequence (carried out at time $t_0$ relative to a fixed origin) involves four signals of the form $\cos(\omega t + \phi)$, and the observed fringe depends on the relative phase $\phi_{00} = \phi_{01} + \phi_{10} - \phi_{11} + \Delta \omega t_0$, where

$$\Delta \omega = \omega_{01} + \omega_{00} - \omega_{10} - \omega_{11}. \quad (1)$$

If the four frequencies are phase-locked and satisfy the energy-conserving condition $\Delta \omega = 0$, the Ramsey output is insensitive to the starting time $t_0$ of the sequence, depending only on $\phi_{00} = \phi_{01} + \phi_{01} - \phi_{10} - \phi_{11}$. We observe Ramsey fringes by adjusting the phase of any of the microwave fields by a variable offset $\delta \phi$, with the $\phi_{00}$ and $\phi_{01}$ fringes off phase with the $\phi_{00}$ and $\phi_{01}$ fringes. A fringe resulting from varying $\phi_{01}$ is shown in Fig. 2c.

The contrast of our mapped Ramsey sequence can be affected by errors in both the population and the phase of the mapping $\pi$-pulses. Population left in the storage states $|0\rangle$ and $|1\rangle$ from incorrect mapping would decrease the contrast of the working-state fringe. However, the transfer efficiency of a $\pi$-pulse is only quadratically sensitive to detuning, giving a small effect for small inhomogeneity. The phase of the mapping pulses also matters, unlike $\pi$-pulses on isolated two-level systems. As the mapped states spend half the time in a field-sensitive superposition during the mapping pulses, the effective field sensitivity during the mapping process is half that of the $|0\rangle + |0\rangle'$ superposition. Thus, despite the fact that the total duration of the mapping...
process (200 μs) is not significantly smaller than the dephasing time $T_2^*$ of the sensitive transitions (∼500 μs), the fringe has high contrast, confirming that the qubit coherence is largely unaffected by the mapping process.

We obtain the necessary field gradients to make the mapping process addressable by generating an optically induced effective magnetic field at every other lattice site, that is, on one site of each of our two-qubit registers, as illustrated in Fig. 3a. This optically induced effective magnetic field is proportional to the local ellipticity of the lattice light, which we control using electro-optic modulators (see the Methods section and ref. 16). The spatially varying effective magnetic field $B_{\text{eff}}$ results from the atom’s vector light shift (which adds to the scalar light shift providing the lattice potential), where $B_{\text{eff}} \sim \alpha_{\text{e}} (E^* \times \mathbf{E})$, $\alpha_{\text{e}}$ is the vector polarizability, $\mathbf{E}$ is the lattice electric field and $E^* \times \mathbf{E}$ is the local ellipticity of the lattice field. $B_{\text{eff}}$ adds vectorially with the external bias field [16,25–27].

We can adiabatically transform the initial $B_{\text{eff}} = 0$ lattice into a lattice with a non-zero $B_{\text{eff}}$ at the B sites of each quantum register, Zeeman-shifting the resonant frequency of the B sites by $\Delta_{AB}/\hbar$. The effective field remains zero at the A sites, resulting in an effective magnetic field gradient between the A and B sites. For a given polarization configuration, this shift is proportional to the lattice-beam intensity as illustrated in Fig. 3b, and corresponds to a field gradient of up to $\sim 8 T m^{-1}$. In the presence of this gradient, the A and B sites of the quantum register can be addressed using radiofrequency or microwave fields. We now demonstrate (1) that our qubits are largely insensitive to $B_{\text{eff}}$, yet (2) we can nevertheless use $B_{\text{eff}}$ to coherently address selected qubits in our quantum register.

The robustness of the storage-state qubit in the presence of the effective magnetic field is illustrated in Fig. 3d. We show high-contrast Ramsey fringes, measured independently for A and B sites, where we apply the addressing field $B_{\text{eff}}$ to the B qubits between the $\pi/2$-pulses comprising the Ramsey sequence. As expected, the storage-state coherence on either site is unaffected by $B_{\text{eff}}$. During the application of $B_{\text{eff}}$, a phase offset of $19(2)^\circ$ develops between the Ramsey fringes of the two sites, which corresponds to a small energy difference of $\hbar \times 35 Hz$ over the 1.5 ms Ramsey delay. This partially results from an intensity difference (and associated difference in differential light shifts) that exists between the A and B sites in the $B_{\text{eff}} = 0$ configuration (see Fig. 3a). To understand this, we measure the magnitude of the differential light shift for the working-state transition, first in the $B_{\text{eff}} = 0$ configuration, and then for the A sites in the $B_{\text{eff}} \neq 0$ configuration, both as a function of intensity, as illustrated in Fig. 3c. We parametrize the lattice-beam intensity in all lattice configurations in terms of the equivalent lattice depth of the $B_{\text{eff}} = 0$ configuration (see the Methods section). Given this parametrization, we measure the differential light shift for atoms in the $B_{\text{eff}} = 0$ configuration to be $6.1(5) Hz/E_R = \hbar^2 k^2/2M = \hbar \times 3.499 kHz$, with $k = 2\pi/\lambda$ and $M$ is the $^{87}\text{Rb}$ atomic mass. This is near a calculated value of 4.9 Hz/E_R based on a model of the lattice and an atomic light-shift calculation. The difference between these curves represents crosstalk: the extent to which the addressing process perturbs A-site atoms, which nominally experience no effective magnetic field. A typical 25 Hz difference in differential light shifts on the A sites (between the $B_{\text{eff}} = 0$ and $B_{\text{eff}} \neq 0$ configurations) combined with a typical 15 kHz effective Zeeman shift of the B sites suggests a crosstalk figure-of-merit for our system of $\sim 0.002$. For the two storage-state Ramsey fringes of Fig. 3d, the estimated difference in differential shifts between the A and B sites of $\sim 12 Hz$ (different from that of the case of the working transition) combined with the $B_{\text{eff}}$ application time of $\sim 600 \mu s$ gives an expected phase shift of $\sim 3^\circ$, considerably smaller than that observed. Several effects could contribute to this discrepancy: drifts in the lattice intensity, peculiarities of beam alignment not included in our lattice model and drifts in both microwave/radiofrequency power and background magnetic fields leading to shifts in the
two-photon transition controlling the storage-state qubits (see the Methods section).

Figure 4 illustrates our full capability, where we combine coherent mapping between storage and working states with the addressing provided by the use of $B_{\text{eff}}$. The combination is complicated by the need to simultaneously satisfy three possibly conflicting criteria: the prevention of ‘leakage’ of the mapped-site population into unwanted hyperfine states (see Fig. 4a) and the assurance that each of the two mapping pulses affects only one site (A–B isolation; see Fig. 4b). As our Rabi frequencies are comparable to both the effective Zeeman shift from $B_{\text{eff}}$ as well as the differential shifts of the hyperfine states due to the nuclear magnetic moment, some care is required. We initialize both qubits in the register with a $\pi/2$-pulse on the storage-state transition, apply the effective magnetic field to the B sites, then apply the mapping pulses. As $B_{\text{eff}}$ shifts the B-site mapping transitions from the A-site resonance (by $\Delta_{AB}/h = 23$ kHz), conversion from storage states to working states is carried out only on the A sites. We satisfy the above three isolation criteria by appropriately choosing three mapping parameters: the effective Zeeman shift $\Delta_{AB}$ and the two microwave Rabi frequencies of the mapping $\pi$-pulses. In particular, the Rabi frequency of the second mapping pulse (|1⟩ → |1′⟩) was chosen to eliminate transitions to closely lying undesired states, exploiting the slight non-degeneracy of the various transitions, as in the global operation of Fig. 2. In addition, we chose $\Delta_{AB}$ such that the second mapping pulse exhibited zero response at a detuning of $\Delta_{AB}/h$. Finally, we chose the Rabi frequency of the first mapping pulse (|0⟩ → |0′⟩) so that it similarly exhibited zero response at a detuning of $\Delta_{AB}/h$. Alternatively, one could use spectrally narrower pulses (such as shaped Blackman pulses) to assure negligible frequency response outside the narrow band of the pulse.

To verify the site-selective mapping of the A-site atoms to the working states, we (1) measure the state population in the A sites after closing the Ramsey sequence with a $\pi/2$-pulse on the working transition and (2) measure the state population in the B sites after a $\pi/2$ pulse on the storage transition. The data shown in Fig. 4 prove the coherence and isolation of the transfer process and also demonstrate controlled single-qubit rotation carried out on only one site of the register. The high contrast of the resulting fringes confirms that the process is coherent, and that state pollution from imperfect A–B isolation or intra-site leakage to undesired states is at most 3% (comparable to our measurement uncertainty of about 3%).
Any control scheme incorporating field-sensitive transitions (as ours does) is vulnerable to imperfections in the quality of the control, owing to fluctuating or inhomogeneous background or control fields. Although our observed global Ramsey fringe contrasts are consistent with unity, scalable quantum computing places stringent limits on required control fidelities. This level of control can be achieved with composite pulses, providing a specific desired result (such as that of the $\pi$-pulses used in our transfer process) using a train of pulses of variable pulse area and phase. Composite pulses are designed to be robust against fluctuations and inhomogeneities over a given bandwidth; $\pi$-pulses of particular interest to the quantum-computing community have been discussed and explored experimentally. As a proof of principle, Fig. 5 shows the results of applying the venerable CORPSE pulse sequence on the field-sensitive transition ($\vert F = 1, m_F = -1 \rangle \rightarrow \vert F = 2, m_F = 0 \rangle$), along with the results of conventional $\pi$-pulses. As expected, the $n$-CORPSE-$\pi$ spectra are significantly flatter about resonance than the equivalent $\pi$-pulse spectra. These are not immediately applicable to our transfer process owing to issues involving A–B isolation, but demonstrate the inherent utility of the technique for neutral-atom quantum computation.

The technique demonstrated here can be used with the effective field gradient of an individual focused laser beam to provide single-site addressing. The ultimate fidelity of such addressable control will be determined by a range of technical issues, such as the stability of the external and control fields, the spatial resolution of the addressing beam and its registration to the lattice position, and the lattice intensity. The fundamental limit is set by the spontaneous photon scattering of the light providing the effective magnetic field gradient. In $^{87}$Rb atoms, for example, one optimal choice for the addressing laser wavelength is found near 787 nm, detuned between the $5^2P_{1/2}$ and $5^2P_{3/2}$ transitions. The total scattering probability during a site-selective $\pi$-pulse depends on the details of the system but we calculate that for a 1 $\mu$m beam waist and 0.5 $\mu$m lattice spacing, the scattering probability can be $\leq 2 \times 10^{-4}$. In the context of our double-well lattice, future work will focus on implementing the transfer process with composite pulses and implementing benchmarking techniques to probe our control fidelities below the per cent level. We also seek to use our techniques to provide all possible inputs to the SWAP gate described in ref. 10, where the relevant gate time is more than two orders of magnitude faster than the relevant coherence time. In a more general context, the approach we have demonstrated here is applicable to any quantum-computing architecture where two appropriate pairs of states can be found, with the attendant ability to transform in and out of a storage-state quantum memory.

**Methods**

We load our optical lattice with ultracold atoms originating from a spin-polarized $^{87}$Rb Bose–Einstein condensate in the $5^2S_{1/2}(F = 1, m_F = -1)$ hyperfine ground state. We produce small condensates with $8 \times 10^8$ atoms (such that the resulting lattice filling factor is near unity) in an Ioffe–Pritchard magnetic trap; to this trap, we subsequently add a three-dimensional optical lattice, generated by intersecting beams from a Ti:sapphire laser operating at $\lambda = 810$ nm. A lattice along $z$ divides the Bose–Einstein condensate into a stack of independent two-dimensional systems, and a separate, deformable double-well lattice formed from a single folded and retroreflected beam in the $xy$ plane completes the confinement. As the total lattice depth in the lattice is a complicated function of the laser polarizations controlling the topology, we parametrize the intensity of the single $xy$-lattice input beam for all lattice configurations in terms of the equivalent $xy$-lattice depth in the $B_{xy} = 0$ configuration. In terms of this parametrization, the total light shift experienced by a trapped atom in the $B_{xy} = 0$ configuration will be approximately twice the $xy$-lattice depth plus the depth of the lattice along $z$. During loading, all lattice intensities follow an exponential profile, reaching their final values in 150 ms (with a time constant of 50 ms). Typical final lattice depths are $20(1)$ $E_h$ for the vertical lattice and $20(1)$ to $40(2)$ $E_h$ for the $xy$-lattice, where $E_h = h \mu k^2/2M = h \times 3.499 \text{ kHz}$, with $k = 2\pi/\lambda$, and $M$ is the $^{87}$Rb atomic mass. (Unless otherwise stated, all
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