Muon-induced background to proton decay in the $p \rightarrow K^+\nu$ decay channel with large underground liquid argon TPC detectors.

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Abstract

Large liquid argon TPC detector programs such as LBNE and LAGUNA-LBNO will be able to make measurements of the proton lifetime which will outperform Cherenkov detectors in the proton decay channel $p \rightarrow K^+\nu$. At the large depths which are proposed for such experiments, a non-negligible source of isolated charged kaons may be produced in the showers of cosmogenic muons. We present an estimate of the cosmogenic muon background to proton decay in the $p \rightarrow K^+\nu$ channel. The simulation of muon transport to a depth of 4 km w.e., is performed in the MUSIC framework and the propagation of muons and secondary particles through to a cylindrical 20 kt LAr target is performed using Geant4. An exposure time of 100 years is considered, with a rate of < 0.0012 events/kt/year at 90% CL predicted from our simulations.

Keywords: Proton decay, Nucleon decay, Muon-induced background, Liquid argon, LAr TPC

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1. Introduction

An attractive framework in which to embed the Standard Model (SM) of particle physics is a Grand Unified Theory (GUT) in which each of the three independent gauge coupling constants of the SM symmetry group $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$ are unified at a high-energy scale, $\Lambda_{\text{GUT}}$. Any GUT model of hadrons, leptons and gauge interactions would necessarily imply the violation of baryon-number conservation at the $\Lambda_{\text{GUT}}$-scale [1]. If one pursues such a theory, the fundamental observables of $\Lambda_{\text{GUT}}$-scale physics would be closely related to the stability of the proton. In particular, the lifetime of the proton and the dominant proton decay products could indicate a preference towards a specific GUT model and could also provide an insight into physics below the $\Lambda_{\text{GUT}}$-scale.

In the simplest extension to the SM, one can extrapolate the three coupling constants to high energies such that the different couplings become the same order of magnitude above $10^{15}$ GeV [2]. One caveat with this procedure is that the couplings do not unify at a single energy scale [3][4] as one might expect from the most simple GUT [5]. The observed stability of protons in the decay mode $p \rightarrow \pi^0\nu$, $\pi^0 \rightarrow \gamma\gamma$ presents another problem for the simplest GUT model. These problems can be avoided in extended GUT models by suppressing or forbidding this decay mechanism. Extended GUT models can incorporate supersymmetry [7] in which the favoured process for proton decay can be $p \rightarrow K^+\nu$ [8], whilst allowing the SM couplings to unify at a single energy scale [3].

Amongst the next generation of high precision proton-decay detectors will be large liquid argon (LAr) time projection chambers (TPC) such as LBNE and LAGUNA-LBNO [9][10]. These experiments will introduce LAr fiducial volumes of the order of tens of kt at depths of at least 1.5 km. LAr TPC imaging will have a higher efficiency to measure the mode $p \rightarrow K^+\nu$ compared to Cherenkov detectors, and as such they will outperform existing detectors such as Super Kamiokande [11]. Given the high efficiency for $K^+$ particle identification in LAr TPC detectors, the largest background to the $p \rightarrow K^+\nu$ signature will be from cosmogenic muons and neutrinos.

In this paper, we present the results of our simulation of the number of backgrounds to this signal from $K^+$ mesons produced in the showers of cosmogenic muons. We compare our results to the study performed by Bueno et al in Ref. [12]. Compared to the latter study, we perform the first full Monte Carlo simulation of particle production, transport and detection that includes cosmogenic muons and all secondary particle [1]. We also consider a depth and scale of the detector volume which is more applicable to the LBNE and LAGUNA-LBNO detectors.

2. Simulation framework

In our model, a LAr TPC detector is positioned at a depth of 4 km w.e., which corresponds to the proposed depths of the LBNE and LAGUNA-LBNO detectors. We model a total mass of 20 kt of LAr, which is close to design specification of the LAGUNA-LBNO detector. The detector is modelled as a cylinder of LAr with a diameter of 30 m and a height of 20 m. The

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LAr cylinder in encased within a stainless steel container with a thickness of 5 cm. One can compare this to the study performed by Bueno et al [12] which reports a prediction of the background rate using a 100 kt volume of LAr at a depth of 3 km w.e. simulated in the FLUKA [13] framework.

The designs of large-scale LAr detectors include up to 2 m of non-instrumented LAr which will separate TPCs from the physical walls. This region of non-instrumented LAr defines a ‘wall’ for this study; as no interaction or energy loss occurring in this volume can be seen by the TPC and is unlikely to be caught by a light detector, unless a very sophisticated light detection system is used. We do not model this region of the detector, and instead treat this boundary as one of the physical walls of the detector.

In this paper, the simulation of particle propagation is performed in two stages. In the first stage, only muon transport is considered and the interactions of secondary particles are neglected. In the second stage, all particles including secondary particles are fully simulated.

In the first stage of the simulation, muons are propagated from the surface of the Earth through a vertical depth of 4 km w.e. using the MUSIC transport code [14, 15]. A simple model of standard rock with proton number Z = 11, nucleon number A = 22 and density ρ = 2.65 g cm⁻³ is used in the muon transport simulation. The overall muon flux normalisation is provided by the Gaisser parameterisation [16], which has been modified for large zenith angles. The muons are then sampled on the surface of a cuboid using the MUSUN code [15].

The cuboid has a height of 32 m and horizontal dimensions of 40 m × 40 m, within which the detector cylinder is centred. The energy spectra of a sample of 10⁷ muons which have been fully transported by MUSIC/MUSUN to the top and sides of the cuboid surface are shown in Figure 1.

The second stage of the simulation is performed using Geant4.9.6 [17], in which all primary and secondary particles are transported from the surface of the cuboid until all surviving particles have exited the cuboid volume. In the second stage of the simulation, all particle information and associated energy depositions in the LAr volume are recorded.

3. Event selection

In this section, we present event selection criteria which maintain high efficiency for selecting p → K⁺ν signal events whilst rejecting cosmogenic muon-induced backgrounds.

Kaons from free proton decay are expected to have a kinetic energy of 106 MeV. After accounting for the Fermi motion of a proton in a nucleus, the nuclear binding energy, and subsequent re-scattering of the kaon, the kinetic energy of a kaon emitted from a nucleus of argon is expected to be smeared across the range 0 to 200 MeV [18]. In a LAr TPC detector, the kinetic energy measurement of charged kaons is further broadened by the energy resolution, which we estimate following the procedure presented in Ref. [19]. In order to retain > 99% of the signal events we require that the energy deposition from a charged kaon due to ionisation and scattering, E_{k,\text{\textsc{dec}}} < 250 MeV.

By constraining the total energy of all proton decay products to the proton mass, we require that sum of E_{k,\text{\textsc{dec}}} and the energy deposition of subsequent decay products, E_{\text{Other}} should be less than 1 GeV. Meanwhile energy deposition from other particles not associated with the kaon, its interactions or decay products, E_{\text{Other}}, in the same event should be smaller than 50 MeV; otherwise this additional energy deposition would be clearly visible.

We reject charged kaon tracks that originate from within 10 cm of a detector wall to ensure that the candidate signal events from proton decay are not mismatched with the events originating outside of the detector. This results in a decrease in efficiency of 2%. We also require that all tracks are not within 10 cm of the detector walls, to ensure for proper energy evaluation and particle identification. Events containing such partially-contained tracks are rejected. The requirement for no activity within 10 cm of the detector wall is shown to reject 87% of events with no primary muons in the fiducial volume.

At the simulated depth of 4 km w.e., we find that muons pass through the LAr detector at a rate of 0.078 s⁻¹, so the average time between the two muons crossing the detector is approximately 12.8 s. Assuming that the maximum drift time, and hence the duration of the event record, will be about 10 ms, the probability of a muon crossing the detector within any 10 ms time window will be approximately 10⁻³. Rejecting events that contain a muon, where the muon’s track length is greater than 20 cm for clear identification, results in the reduction of p → K⁺ν detection efficiency of about 0.1%.

LAr TPC detectors can identify charged kaons in the range of interest (< 250 MeV) via their dE/dx in LAr [19]. For low energy charged kaons the identification efficiency is assumed to be 100%, which will lead to a slightly conservative estimate of the background to p → K⁺ν. In order to fully account for the kaon identification efficiency, detailed studies will need to be performed for each specific detector design. Although it is assumed that this method can identify charged kaons with a high efficiency, using dE/dx provides no separation between K⁺ and

\[2\] The Geant4.9.6 ‘Shielding’ physics list is used, and the muon-nuclear interaction process is additionally switched on.
$K^+$ states. The following procedure will provide some degree of separation. By considering the dominant $K^+$ decay modes, one would expect to find a $\mu^+$ in 95% of $K^+$ decays, either directly from the $K^+$ or via a subsequent $\pi^0$ decay. In these decay modes, $K^+$ and $K^-$ can be separated in the event of either $\mu^+$ or $\pi^0$ capture in the liquid argon. Before considering the muon capture lifetime, the procedure of identifying positive kaons as having a decay chain which features $\mu^+ \rightarrow e^+$ would reject 95% of negative kaons. After comparing the muon capture lifetime in argon [20] to the muon lifetime [21], the $K^+$ rejection factor is reduced to 82%. In addition to $K^+$ decay chains featuring $\mu^+ \rightarrow e^+$, we also permit events featuring $K^+ \rightarrow e^+X$ (where $X$ is any other set of particles) in order to account for the remaining 5% of $K^+$ decays.

To summarise, we propose the following selection criteria for $p \rightarrow K^+\nu$ events in large LAr TPC detectors:

1. There is exactly one $K^+$ in the event.
2. There are no muons with track length $> 20$ cm in the detector volume.
3. There is no activity within 10 cm of the detector wall.
4. The $K^+$ decay chain includes the decay $\mu^+ \rightarrow e^+$ or $K^+ \rightarrow e^+X$, for electrons with $E_e > 5$ MeV.
5. The total energy deposited by the $K^+$, excluding decay products, satisfies $E_{\text{int}}^{K^+} < 250$ MeV.
6. The total energy deposited by the $K^+$ and by $K^+$ decay products, satisfies $(E_{\text{int}}^{K^+} + E_{\text{dec}}^{K^+}) < 1$ GeV.
7. The total energy deposited in the rest of the fiducial volume satisfies $E_{\text{Other}} < 50$ MeV.

4. Results

In total, an exposure time of 100 years has been simulated. The number of events that are expected to pass the sequential selection criteria described in Section 3 is presented in Table 1. After applying all cuts, we do not observe a single muon-induced $K^+$ event in our simulations. Figure 2 shows the distribution of $E_{\text{int}}^{K^+}$ and $E_{\text{Other}}$ for events with charged kaons after applying cuts 1 - 4, as specified in Section 3. The region retained by the respective selection criteria for both $E_{\text{int}}^{K^+}$ and $E_{\text{Other}}$ are applied, is bound by the blue-dashed lines. It is found that even if the requirement on the kaon kinetic energy is loosened such that $E_{\text{int}}^{K^+} < 400$ MeV, there will be no events in the region of interest.

We find that the main source of events $K^+$ events is due to the production of $K^0_L$ outside of the LAr TPC volume. For events passing the selection, the $K^+$ ionisation energy peaks below 200 MeV, but these events are rejected by requiring that the total energy deposition not associated with the charged kaon is lower than 50 MeV.

The absence of a single muon-induced $K^+$ event from our event selection is converted to an 90% Confidence Level (CL) upper limit of 0.024 background events per year in a 20 kt liquid argon detector, or 0.0012 events/kt/year. This result is consistent with earlier estimates [12]. The presented event selection reduces the efficiency for $p \rightarrow K^+\nu$ selection by less than 2%, which is dominated by the requirement for no activity within 10 cm of the detector wall.

5. Conclusions

We have presented an estimate of the muon-induced background to proton decay in LAr TPC detectors. We consider the background to the process $p \rightarrow K^+\nu$, which is favourable in extended GUTs models.

In our simulation, a cylindrical LAr TPC detector is positioned at a depth of 4 km w.e., which corresponds to the depths of the proposed LBNE and LAGUNA-LBNO detectors. We consider a total mass of 20 kt of LAr, which is close to design specification of the LAGUNA-LBNO detector.

We find that the main source of muon-induced background $K^+$ events is due to muon-induced $K^0_L$ mesons produced outside of fiducial volume. We show that background $K^+$ events can be rejected by constraining to the kinematics of the proton decay as well as requiring that the total energy deposition in the event not associated with the $K^+$ is less than 50 MeV and that there is no activity within 10 cm of the detector wall.

After considering an exposure time of 100 years, we set a 90% CL upper limit on the number of background events as 0.0012 events/kt/year. Furthermore, the presented event selection is estimated to reduce the signal efficiency by less than 2%, which is dominated by the requirement for no activity within 10 cm of the detector wall.
Table 1: The number of expected events after 100 years of exposure, as a function of sequential selection criteria and the $K^+$ production mechanism. Events are accepted into the table if the total energy deposition in the event is less than 2 GeV. Numbers presented in brackets indicate the subtotal number of $K^+$ events. $N$ refers to nucleons in the interaction.

| $K^+$ parent | Exactly one $K^+$ | No muon | No activity near wall | $(\mu^+ or K^+ \rightarrow e^+ + X)$ | $E_{K^+}^{Int} < 250$ MeV | $E_{K^+}^{Int} + E_{Dec} < 1$ GeV | $E_{Other} < 50$ MeV |
|-------------|------------------|---------|----------------------|---------------------------------|------------------------|-------------------------|------------------------|
| $\mu^+ + N$ | 255 (43)         | 59 (10) | 0                    | -                              | -                      | -                       | -                      |
| $\pi^+ + N$ | 134 (20)         | 79 (14) | 3 (0)                | 3                              | 3                      | 3                       | 0                      |
| $(\pi^0 + N$ | 13 (2)           | 7 (1)   | 0                    | -                              | -                      | -                       | -                      |
| $\gamma + N$ | 8                | 6       | 0                    | -                              | -                      | -                       | -                      |
| $\Sigma^-$  | 1                | 1       | 0                    | -                              | -                      | -                       | -                      |
| $(n/n) + N$ | 11 (1)           | 9 (1)   | 0                    | -                              | 24                     | 24                      | 0                      |
| $K^0_{S\bar{S}}$ | 12 (2)        | 10 (1)  | 0                    | -                              | -                      | -                       | -                      |
| Total       | 552 (96)         | 234 (42)| 34 (2)               | 34 (0)                         | 27                     | 27                      | 0                      |

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