The Best Trail Algorithm for Assisted Navigation of Web Sites

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ABSTRACT

We present an algorithm called the Best Trail Algorithm, which solves the hypertext navigation problem by automating the construction of memex-like trails through the corpus. The algorithm performs a probabilistic best-first expansion of a set of navigation trees to find relevant and compact trails. We describe the implementation of the algorithm, scoring methods for trails, filtering algorithms and a new metric called potential gain which measures the potential of a page for future navigation opportunities.

1. INTRODUCTION

The World Wide Web is a massive global hypertext system in which documents (or pages) can be found on almost every subject imaginable. These pages are made available by many authors and written in many languages. We consider a web site to represent a collection of pages with some common element, such as topic, author or institution. The process of navigation or surfing is that of following links according to the topology of the web site and viewing (or browsing) the contents of visited pages. During the navigation process users may become "lost in hyperspace", meaning that they become disoriented. This happens when users fail to understand the context of the pages they are viewing, are unsure of how they reached a page, cannot see how the page is related to key pages such as the homepage or are uncertain as to where they should proceed to find the information they are looking for.

Vannevar Bush envisaged a hypothetical machine called a memex [1] - a cabinet-like box into which the user could store documents and images. A sequence of such documents could then be annotated and linked together to form a trail. By continuing the process, Bush imagined that future workers could build a "web of trails".

In Berners-Lee’s Web, a trail or navigation path is implicitly formed as the result of a navigation session in which the user visits a sequence of web pages. Previous research [7] has shown how the trails which users follow can be extracted from log data. Often the starting point for one of these trails is a page resulting from a search request [29], yet existing site search engines will neither consider the possibilities for future navigation when returning their result nor present details of the paths users might follow.

It is our hypothesis that constructing trails or paths in a query-dependant manner will provide contextual information that will reduce the effects of the navigation problem and increase user-satisfaction during search tasks. Our contribution is to describe a probabilistic best-first algorithm for automating the discovery of memex-like trails from a set of starting points. We describe metrics for evaluating trails, and introduce a new metric for determining more effective starting points by evaluating the potential gain of future navigation from a given page. Previous hypertext systems have featured the ability to manipulate trails manually [12, 30, 33] or allowed the construction of trails using pure IR metrics [4, 16]. However, none of these systems has allowed the automatic construction of trails by the computer in any way that takes account of hyperlinks.

The rest of this paper is organized as follows: In section 2 we describe our system for computing trails - selecting starting points using the potential gain metric, expanding the trails using the Best Trail algorithm and filtering redundant information from them with heuristic methods. In section 3 we describe our preliminary efforts to evaluate the utility of the navigation engine which uses these trails to assist users [21]. In section 4 we describe our implementation of the algorithm. In section 5 we describe experiments into the behaviour and performance of this implementation. We discuss related work in section 6 and give our concluding remarks and directions for future research in section 7.

2. COMPUTING TRAILS

In this section we outline our methodology for computing trails. Trails are computed by selecting relevant starting points, expanding a navigation tree from each node using the Best Trail algorithm before filtering and sorting the resulting set of trails.

We view a web site as a hypertext system $H$ having two components: a directed graph $G = (N, E)$, having finite sets of nodes and edges $N$ and $E$, respectively, and a scoring function $\mu$ which is a function from $N$ to the set of non-negative real numbers. The directed graph $G$ defines the web site topology and is referred to as the web graph; the nodes in $N$ represent the web pages and the edges in $E$ represent hyperlinks (or simply links) between anchor and destination nodes. Figure 1 shows an example web graph, taken from the GraphViz web site [1], which we will use as...
a running example. The terms node, web page and URL will be used interchangeably. We interpret the score, \( \mu(m) \) of a web page \( m \in N \), as a measure of how relevant \( m \) is with respect to a given query, where the query is viewed as the goal of the navigation session. The Best Trail algorithm computes trails scored by a function of these page scores.

2.1 Selecting Starting Points

Whilst simply expanding from relevant points is effective, we can do better by considering future navigation opportunities in our starting point selection. We have created a metric for finding good starting points which we refer to as the potential gain of a url. That is, the potential for future navigation opportunities. Defined as the sum for all depths of the product of the fraction of trails to that depth, \( d \) and the discounting function \( f(d) \), it is easily computed by an iterative algorithm or by a series of matrix operations. For larger graphs, we can utilize similar techniques to those proposed for the PageRank citation metric. For our experiments, we compute potential gain using the reciprocal function, \( f(x) = x^{-1} \).

When restricted to a maximum depth of traversal, \( d_{\text{max}} \) the naive algorithm takes time proportional to \( O(d_{\text{max}}.|E|) \) and space proportional to \( O(|N|) \) to compute potential gain values for all nodes in \( G \) given that \( G \) is sparse. In practice, after a brief settling period, convergence to a set of potential gain values occurs in a short space of time. Bucketed values for potential gain follow a power-law distribution, as is found for PageRank and many other web-related phenomena.

2.2 The Best Trail Algorithm

The pseudo-code of the Best Trail algorithm is shown in figure 2. It takes as input a set of starting URLs, \( S \), and a parameter, \( M \geq 1 \), which specifies the number of repetitions of the algorithm for each input URL. When the algorithm terminates it outputs a set of trails, \( B \). There are \( M \) trails in \( B \) for each URL in \( S \). Each trail is the highest ranking trail contained within the navigation tree expanded from a single starting node. A navigation tree is a finite subtree of the possibly infinite tree generated by traversing through \( G \), the root of which is a member of the set of starting points. Manipulating sets of navigation trees has a filtering effect on the set of starting points, reducing the rank of nodes which are isolated from other relevant documents and from which navigation is problematic. Returning trails from separate trees also has the effect of removing highly similar trails before further filtering is required.

Starting from each node in \( S \), the algorithm follows links from anchor to destination according to the topology of the web site. At each stage of the traversal, one of the tips (the leaf nodes of the navigation tree) is chosen for expansion. The destination node of each outlink whose source is represented by the chosen tip is assigned a new tip which is added to the navigation tree, along with a computed trail score. Previously visited nodes in the web graph will result in distinct nodes in the navigation tree, with identical page scores but different trail scores. Figure 4 shows an example navigation tree based on the web topology shown in figure 1.

The algorithm has a main outer for loop which computes the best trail for each URL. The second loop recomputes the best trail \( M \) times. The two innermost loops comprise the exploration and convergence stages of the algorithm, both of which expand the navigation tree - from which the best trail is selected by the \( \text{best}() \) function. The number of iterations in the exploration phase is set by \( I_{\text{explore}} \), whilst the number of iterations in the convergence phase is set by \( I_{\text{converge}} \). During the exploration phase, the \( \text{select}() \) function selects a tip to expand where the probability of a tip \( t \) being selected is given by

\[
P(D_i, t) = \frac{\rho(t)}{\sum_{k=1}^{n} \rho(t_k)}
\]

where \( \rho \) is a scoring function for the trail, making the probability of any node being selected directly proportional to its score. During the convergence phase, the probability of a node \( t \) being selected is dependant only on its relative rank, \( \tau(t) \), in the ordered set of candidate tips, and is given by

\[
P(D_i, t, df, j) = \frac{df^{\tau(t)}}{\sum_{k=1}^{n} df^{\tau(t_k)}}
\]

where \( j \) is the number of completed convergence iterations and \( 0 < df < 1 \) is a discrimination factor. The discrimination factor allows us to discriminate between “good” trails and “bad” trails by reducing the influence of trails with low scores. Thus during the convergence stage “better” trails get assigned exponentially higher probability. Setting \( df \) equal to 1 would imply a uniform random selection, whilst as \( df \) tends towards 0, the behaviour of the algorithm tends towards that of a best-first approach. The degenerate case of the Best Trail algorithm where \( df = 0 \), \( I_{\text{explore}} = 0 \) and \( I_{\text{converge}} \geq 0 \) is equivalent a simple best-first algorithm. The rank of a tip, \( t \), (or of the trail leading to it), denoted by \( \tau(t) \), is determined by the tip’s position within the ordered set of candidate tips. The position of \( t \) is determined by comparing trails based upon

1. The number of query terms matched by the trail ending at \( t \).
2. The maximum number of query terms matched by any single page in the trail.

![Figure 2: The Best Trail Algorithm. The algorithm takes two arguments. \( M \) is the number of repetitions and \( S \) is a set of starting URLs.](image-url)
The trail score, $\rho(t_k)$.

It has been argued that the number of keywords in a query that are matched by a document should take precedence over other scoring mechanisms, and that the terms for a query may be spread across several pages \[2, 26, 18\]. Ranking the other scoring mechanisms, and that the terms for a query should take precedence over the number of keywords that are matched by a document should take precedence over the number of pages indexed. The numbers in parentheses denote relevance scores for the query “dotty”.

2. The discounted sum of the scores of the URLs in the trail, where the discounted score of $U_i$ is the score of $U_i$ multiplied by $\gamma$ and raised to the power of $i - 1$, where $0 < \gamma < 1$ is the discount factor.

3. The weighted sum of discounted scores, where the additional weighting is achieved by discounting each URL according to its previous number of occurrences within the trail. The weighted score of $T$ is given by:

$$
\rho(T) = \text{weighted}(T) = \sum_{i=1}^{n} \mu(U_i) \gamma^{i-1} \delta^{c(i)}
$$

where $c(i) = |\{U_j | j < i \land U_j = U_i\}]$ and $\delta$ is a second discounting function, which reduces the importance of nodes with equal content. We note that although $i = j$ implies $U_i = U_j$, $U_i = U_j$ does not imply $i = j$. Two distinct nodes may be considered equal if they have equal content, determined in advance using checksum of page contents and comparing likely candidates. This definition of node equality can easily be extended to near-duplicate documents \[8, 35\].

Figure 4 shows examples of score shows how the trails in the navigation tree (figure 6) would be scored after two expansions (of tips 1 and 3). The examples shown in this paper are constructed by computing two trails from each starting point - one scored using the sum distinct metric and one using the weighted sum.
Figure 3: An example navigation tree based upon the site structure shown in figure 1. Each node is annotated with a unique tip id, a URLid, with the corresponding URL also shown. Red ellipses denote candidate tips for expansion. The tip numbers are assigned in sequence during the iteration of the algorithm. In this example, the tips numbered 1, 3, 9, 5 and 24 were expanded.

| Tip | Weighted Sum | Sum Unique |
|-----|--------------|------------|
| 1   | 1.8076       | 0.9038     |
| 2   | 3.2593       | 1.2477     |
| 3   | 6.5056       | 2.6905     |
| 4   | 1.8076       | 0.6025     |
| 5   | 3.6534       | 1.4230     |
| 6   | 1.8076       | 0.6025     |
| 7   | 1.8076       | 0.6025     |
| 8   | 1.8076       | 0.6025     |
| 9   | 7.5940       | 2.5018     |
| 10  | 6.5056       | 2.0179     |
| 11  | 6.5056       | 2.0179     |
| 12  | 6.9194       | 2.2018     |

Figure 4: Table showing trail scores using Weighted Sum and Sum Unique. Example trails scores. The high score associated with the first trail has a useful control in forcing the most relevant pages to the forefront of the display. Merging trails with common roots gives a good ordering to the display, as can be seen in figure 5.

2.4 Sorting and Filtering

The returned set of trails is unsorted and may contain redundant information. To sort the trails would appear to be trivial - we simply apply the same rules of sorting by number of keywords matches and then by the trail score. However, we have more than one mechanism for scoring trails, and we can compute trails in different navigation trees using different functions. We can sort the resulting trails using a set of scoring functions, $F$, by specifying that a trail, $T_1$ should be ranked higher than a trail $T_2$ if:

$$\sum_{f \in F} \frac{f(T_1)}{f(T_1) + f(T_2)} > \sum_{f \in F} \frac{f(T_2)}{f(T_1) + f(T_2)}$$

We can improve results by removing redundant trails and redundant sections within trails. To achieve this, we need to define precisely what is meant by a redundant trail. We say that a trail $T_1$ subsumes a trail $T_2$ if and only if all the pages in $T_2$ are contained in $T_1$. A trail, $t_1$ is removed from a result set, $r$ if and only if there exists a trail $t_2 \in r$ such that $t_2$ subsumes $t_1$ and $\rho(t_2) > \rho(t_1)$. Within a trail $T$, we consider a page, $t_i$ to be redundant if and only if the page can be removed whilst still leaving a valid trail through the web site topology (i.e. if $t_i$ is the last node of the trail or $(t_{i-1}, t_{i+1}) \in E$ and the information contained on page $t$ is either not relevant or contained in a previous page (i.e. if $\rho(t) = 0$ or $\exists j t_j = t_i \land j < i$). These definitions were arrived at as the result of several experiments and typically remove trivial reorderings and irrelevant content.

Finally, the trails with common roots are merged into a tree and presented in the NavSearch UI [24], shown in figure 8. Two other interfaces have been developed for displaying these trails - a flat TrailSearch interface similar to that used by traditional search engines for displaying linear results and a GraphSearch interface which displays the results in the form of a graph [41].

3. EVALUATION

3.1 A Case Study

A case study was performed into the use of the navigation engine on the Birkbeck School of Computer Science and
Information Systems (SCSIS). Queries were taken from a recent log file and analysed. The chief results of the analysis are presented along with examples.

The trails provide relevant information. For example, results for the query “andrew” find the home pages of Andrew Bielinski, Andrew Watkins and Andrew Mair. For the query “application form”, the first trail identifies the application form for the MSc E-Commerce course and the second identifies the application form required for the undergraduate program (figure 4). The first two trails for the query “xml”, shown in figure 7, give brief tours of an XML tutorial, always linking to external resources containing a great deal of relevant information. The third trail provides an explanation of XML namespaces connected to hub with lots of XML references. The use of Potential Gain in the starting point selection encourages such hubs to be chosen. The fourth trail details the use and history of XML as a markup language and its relationship to SGML. Subsequent trails describe the Information Technology (IT) applications module on XML.

However, relevant content can be found with conventional, linear, search engines. More important is that the trails provide context to show associations and to help disambiguate the meaning of keywords and page descriptions. For example, the structure of the trails for the query “andrew” shows Andrew Bielinski to be a research student under the supervision of Mark Levene and that Andrew Mair is (although not a member of the department) associated with the BSc Information Systems and Management course. Similarly, for the query “neural network”, the first trail shows the course “Artificial Intelligence & Neural Networks” linked to the home page of Chris Christodoulou who teaches the course. Chris Christodoulou is the SCSIS expert on neural networks. The second trail leads from his home page to the only one of his papers, “A Spiking Neuron Model: Applications and Learning” linked to from his home page. The user posing the query “exam papers” was almost certainly a student looking for past papers for revision. Figure 8 shows that the first two trails provide exactly that. The second trail shows that the papers relate to the module “Developing Internet Applications”. There are surprisingly few past papers available on the SCSIS site and the remaining trails for this query details relating to arrangements for sitting exams for that summer. The context provided by the trails makes it easier to distinguish between the two types of result.

Unfortunately, the contextual information can be lost when inadequate short titles are presented to describe the pages. For example, in figure 7 it is impossible to tell any differences between the page which share the title “IT APPLICATIONS”. Similarly, for the query “accomodation” (sic.), there are many different pages shown in the trails, all of which relate to the Web Dynamics workshop and contain the search term, but there is no means to discriminate between them. The authors of the pages made no changes in the h1 or title tags by which to identify the differences. The most appropriate title is contained in a later h3 tag.

The query “accomodation” also highlights another major problem - spelling errors are not corrected. Minor user errors or parsing errors in the software introduce significant errors in the presented trails. Similarly, examples such as “birkbhol programmes”, “infirmation systems” and “Information En-ginerring” highlight the failure of users to construct meaningful, accurate queries [37].

Overall, the filtering operations appear to work well at reducing redundant information without destroying contextual information. However, redundant information appears commonly when near-duplicate documents cause separate, highly similar, trails to be created. For example, in figure 6 pages entitled “IT APPLICATIONS” are distinct but differ only by the inclusion of an irrelevant “assessment” section. This small difference causes the creation of 2 separate trails. This can be fixed with the application of near-duplicate detection algorithms [8, 35].

The link structure can be broken when the crawler-based engine fails to identify all the possible links. This can hap-
pen for several reasons - malformed URLs, conservative robot exclusion policies, javascript links and CGI forms. For example, the link between the student person page of Andrew Bielinski's home page is missing, as are the links from all pages in the SCSIS site to the home page, news, courses, research and seminars pages. Similar behaviour found with the output of Content Management Systems (CMSs) such as Vignette or Documentum. The long-term solution to this problem is to tie the trail engine into a better IR system and offer interfaces to the main CMSs. For the current research prototype this is not feasible, but would be essential if the navigation engine was to be developed fully.

The conclusion that can be drawn from this analysis is that the trails found by the navigation engine are useful, but the overall utility of the system is being limited by problems with related modules - namely IR, near-duplicate detection and short title generation. Given all these problems, the overall performance of the system is highly promising. However, to truly test the system's effectiveness requires an independent test with real users.

3.2 A User Study

In order to assess the usefulness of the NavSearch interface and prove the hypothesis that “a trail-based search and navigation engine improves users' navigation efficiency”, Mat-Hassan and Levene conducted a usability study. The results they obtained from the study revealed that users of the navigation engine performed better in solving the question set posed than users of a conventional search engine.

Users were given two sets of information seeking tasks to complete based upon the pages in UCL's official Web site. Three different search tools were evaluated, one of which was the navigation engine with the NavSearch interface. The others were Compass (UCL’s official site search engine) and Google's university search of UCL. Subjects were asked to answer two sets of questions, designed to be at the same level of difficulty, using either NavSearch and Google or NavSearch and Compass. The question sets were formulated so that all the questions fell within one of five types: fact finding, judgement questions, comparison of fact, comparison of judgement and general navigational questions.

Most of the subjects assigned to use Google were more optimistic about the initial likelihood of completing the task, whilst those subjects assigned to use NavSearch were initially more reserved and pessimistic. None of the subjects had any previous experience with NavSearch and familiarity was identified as the main factor in favour of Google's linear interface model. Users were reported to have “found the interface quite intimidating” considering it a “radical shift” from the conventional layout and format of results.

The interfaces were assessed according to users' completion time, the number of clicks employed, the number of correct answers found by the subjects and the confidence and satisfaction levels expressed by the subjects. When asked to compare NavSearch with Google or Compass, subjects expressed a much higher degree of confidence in their ability to complete future tasks, a higher degree of satisfaction with NavSearch with regards to the completion of tasks and a higher degree of satisfaction completion with regard to navigation and the display of results. Users stated that “showing link relationship helps” and that the system provided “useful trails” which gave “an indication of the pages already looked at and the pages that might be useful to look at”. 96% of the study's subjects chose NavSearch over Google.
and Compass as their preferred search engine. Mat-Hassan and Levene concluded that “the proposed user interface does indeed provide effective information retrieval assistance”.

4. IMPLEMENTATION

In this section we give a brief outline of the architecture required to support trail finding and details of the algorithm’s implementation.

Each node, page or URL is assigned a unique ID. IDs are 32-bit signed integers assigned in sequence (from 1) to each URL such that any two identical URLs will have an identical ID. The mapping between URLs and IDs is performed using Berkeley DB files. Each page is associated with a relevance score, determined using tf.idf measures although they may be computed using any information retrieval metric. Given a set of relevances and a graph in this form, we compute the best trails by running the traversal form, we compute the best trails by running the traversal stages in a separate threads for each starting point.

There are many ways to access relevance data in constant time - either through array lookups or hashtables, depending on the size of the webcase. The graph is stored using the URL ids as references. Many strategies have been presented for accessing sets of inlinks and outlinks from large graphs with appropriate time-space trade-offs. At each step of the expand and converge process we must select a tip for expansion based upon the probability distribution described in section 2. These distributions have been carefully selected to allow the use of binary trees for storing this trail score information. We can implement this efficiently by using a table describing the tip selection tree at each stage, reducing the object creation overhead. Associated with each tip is a vector of all relevances for all descendants, denoted as the subscore, s, and the total number of descendants which are referred to as the subcount, c. Figure 9 shows the table storing the tips of the navigation tree shown in figure 3.

4.1 Complexity

It has been shown how the step select(D_i, df_i) can be implemented to run in time O(log(n)) where n is the number of candidate tips. The function best() has the same time complexity, but is slightly simpler in that each iteration is to the left of the current node. Hence, the worst case complexity of algorithm 1 using this implementation can be given as O(KMI\beta^2) where I = I_{explore} + I_{converge} and \beta is the maximal outdegree of any link in E. This can be broken down as follows:

I as the worst-case insertion time for a tip. This factor emanates from the fact that the tree of tips may become a linked list if all new tips are added to the same part of the tree. This might occur in the simple case of nodes having identical scores, so these scores are biased using tiny random numbers to adjust the rank. The magnitude of these adjustments means that they affect only the speed of the operation, not the end results.

\beta representing the number of potential tips which may be added to the candidate set at each iteration. This number would always be added on a fully connected graph, but graphs based upon Web data are very sparse and this will never occur in practice.

KMI as the maximum number of iterations the Best Trail may take to find the given trails.

In practice the tree of tips is unlikely to be skewed to such a degree. Nor is the graph likely to be fully-connected. However, if the average-case complexity is performed by substituting the average outdegree, the results are still inaccurate. Using the weighted average outdegree better models the expansion of the navigation tree during the expansion and convergence phases. The weighted outdegree, \textit{W}, of a node, \textit{n}, is defined as the product of the number of outlinks \((n, x)\) from that node and the proportion of links in the graph which point to that node \([n, y \in E] / |E|\). It is assumed that all links are as likely to be followed as any others, given a sufficient number of queries. It should be noted that, when expanding a navigation tree, the number of potential trails to a depth of \(d\) is roughly equal to \(\sum_{i=d}^{\infty} w_i\), where \(w\) denotes the weighted average outdegree of a graph. Given that \(\beta\) is the weighted average outdegree, the average case complexity can be given as \(O(KMI\beta \log(1/\beta))\). Using binary trees the average-case complexity of the expand operation is \(O(\beta \log M)\) since there are, on average, \(\beta\) elements to be added to the list of candidate tips and the complexity of

\[
\frac{y^k}{\sum_{k=x}^{\infty}} a_k = \frac{y^k(1-a^{y-k+1})}{1-a}
\]

Figure 9: Table showing candidate tips for expansion. SS is the sum of the scores for the current node and all descendants and SC is the number of active nodes reachable from that node. It should be noted that the nodes in this tree represent tips and should not be confused with either the nodes of the graph or the navigation tree produced by the Best Trail.

When selecting a tip to expand, a random number between 0 and \(x\) is selected where either \(x\) is the subscore or

\[
x = \sum_{k=0}^{c-1} df^k (tk)_j^k
\]
operation to insert these new candidates is equal to that of the select function - $O(\log 3I)$.

5. EXPERIMENTAL RESULTS

We have conducted numerous experiments to test the behaviour of the algorithm and explore the effect of the various parameters which control it. These were mostly performed on crawls of the Birkbeck website, the school of computer science and information systems website and the JDK 1.4 javadocs, primarily due to the abundance of query information available to us.

Behaviour of the algorithm is controlled by the parameters $d_f$, $I_{\text{explore}}$, $I_{\text{converge}}$, $M$ and the set of starting points $\{U_0, U_1, \ldots, U_K\}$. As we would expect, increasing the value of either of the parameters $I_{\text{explore}}$ or $I_{\text{converge}}$ produces higher scoring trails on average (figure 10). Unsurprisingly, increasing $I_{\text{converge}}$ finds the local limit of the trail score faster than increasing $I_{\text{explore}}$, as shown by the sharp rise at the very start of the curve. Perhaps more surprising is the behaviour when altering the ratio between $I_{\text{explore}}$ and $I_{\text{converge}}$. Increasing $I_{\text{explore}}$ whilst decreasing $I_{\text{converge}}$ increases the scores of the resulting trails if we measure the relevance using sum distinct but decreases the trail score when calculated using the weighted sum (figure 11). The balance between the values $I_{\text{explore}}$ and $I_{\text{converge}}$ can be tuned to reflect the importance of the two metrics. Increasing the value of $M$ is less effective, as repeated exploration from the same node causes many of the expansions to be duplicates of those performed in other trees. We can use the multi-treaded environment better by expanding from a greater number of starting points, as shown in figure 12.

Figure 12: Increasing the number of starting points increases the score for trails, by allowing a greater number of opportunities for discovery. Trail sets are truncated to the same size.

In order to evaluate the effectiveness of the Potential Gain metric in improving trail scores, we analysed the scores of trails found by traversing the graph from starting points selected by combining the $t.f.d.f$ IR measure, $\mu(p)$, of a page $p$ with the page’s potential gain, $P_g(p)$ in several different ways. Comparisons were also made to test the effectiveness of a simple outdegree count, $Out(p)$ and of Kleinberg’s hub metric [20]. The results showed that, relative to the baseline of selecting according to $\mu(p)$, a significant improvement is achieved by taking the highest scoring pages when scored using $\mu(p)P_g(p)$ or $\mu(p)\log P_g(p)$. Surprisingly, the simple metric $\mu(p)\log Out(p)$ also performed well for the task of starting point selected whilst Kleinberg’s metric performed badly.

6. RELATED WORK

Many graph traversal and path-finding algorithms have been developed over the last 50 years and it is not unreasonable to question the development of a new one. We will consider the effects of a few of them. A depth-first traversal, for example is unsuitable for trail finding as it may tend towards “black-holes” from which there is no escape. It is considered unsuitable for crawling for similar reasons. Breadth-first search is non-viable for anything other than very short trails, due to the exponential growth of the tree. A best-first search is possible but will struggle in situations where the best pages are separated by content which is less relevant - exactly the situations where automated navigation is most needed! Another approach that has been used effectively for computing solutions to the Travelling Salesman Problem (TCP) is Ant Colony Optimization (ACO) [18]. Each “ant” is an agent which uses a greedy heuristic to follow a trail based upon the weight of links and the presence of a “pheromone”. This pheromone is laid by ants following a path, based upon the length of the final result. Our own experiments have provided anecdotal evidence that the Best Trail algorithm out-performs ACO for web-site trail finding, although the ACO system appears to out-perform the Best Trail in finding solutions to TSP.

Several systems have allowed the manual construction of trails. Sillitoe et al. [30] proposed a system for manipulating trails, complete with forks and subtrails. They discussed a database backed scheme for storing and retrieving the information. Furuta et al. [15] developed a system for authoring modifying and re-using Walden’s paths - guided tours which could be used in a teaching environment. WebWatcher advises users on navigation possibilities by highlighting links as they browse. This forms a trail over time, but the link-at-a-time approach does not allow the user to see the context initially. We agree with Joachims et al.’s belief that “in many cases only a sequence of pages and the knowledge about how they relate to each other can satisfy the user’s information need”, but extend this to compute and show complete sequences in advance. Bernstein’s approach to constructing trails was to ask the user to “choose an interesting starting point and ask the apprentice to construct a path through related material”. The tours were constructed via a best-first page finding scheme using document similarity measures [17].

The concept of Information Units, presented in [26] also attempts to break away from the single page model, returning small clusters of linked pages answering the user’s query. The returned units may be more compact than the trails returned by the best trail, and cover situation which cannot be handled using trails, but the returned results are not navigable, nor has there been sufficient consideration to the display of the results and subsequent user interaction. The Cha-Cha system [19] presents results in a similar manner to the NavSearch interface and shows results in context, but the scoring is only conducted at the page level, the trails leading to the page are chosen as the shortest paths, not those with informative content.

Several metrics have been proposed for selecting nodes in search results which relate to the issue of starting point selection. The most famous, the PageRank citation [30] only considers the effect of incoming links, whilst Kleinberg’s Hubs
Figure 10: Increasing either (a) the number of exploration iterations or (b) the number of convergence iterations, increases the score of the returned trails. When increasing $I_{\text{explore}}$, the algorithm slowly tends to a limit, whilst exploring the solution space. When increasing $I_{\text{converge}}$ (and leaving $I_{\text{explore}}$ constant e.g. 0 as in this example), the algorithm quickly tends to a limit.

Figure 11: Increasing $I_{\text{expand}}$, whilst decreasing $I_{\text{converge}}$ increases the resultant trail score when calculated using sum distinct but decreases the resultant trail score when calculated using the weighted sum. The graphs show values for $0 \leq I_{\text{explore}} \leq 100$ where $I_{\text{converge}} = 100 - I_{\text{explore}}$.

and Authorities metrics and extensions of it only consider the effect of single links in each direction, whilst potential gain will consider the effect of more distant pages [20][22].

7. CONCLUSIONS AND FUTURE WORK

We have presented an algorithm for finding trails across the graph of linked pages in a web site. Inspired by Bush’s “memex”, these trails provide a structure to the returned results and provide users with contextual information not provided by traditional search facilities.

Although site-search is of vital importance, and deserves special attention as an area of research separate from global search engines, it would be highly beneficial to allow full web-scale trail finding. Unfortunately, the current architecture will not scale to full-size web data. However, we can break the problem down. Conventional search engines do not index the full content of the web. They select some subset to index based on usage statistics, link analysis or the output of dedicated crawling algorithms designed to select high-quality nodes first [31][32]. We can select a subset of this on which to perform trail computation. For example, we could compute trail information on high-profile or highly-popular sites and return single-page results for the remaining indexed pages. An alternative strategy is to construct a restricted graph based upon the search results for a given query, over which trails could be constructed. Whilst this approach would suffer less scalability problems, it might suffer similar performance issues to Kleinberg’s approach of expanding the search results [20].

The work presented here has many applications in other, non-hypertext areas. We have built a system called DbSurfer, which applies these ideas to solve the join discovery problem in relational databases by finding trails through the graph of foreign key dependencies. We have also built systems for finding trails in program documentation [41] and source code. In this last example, the results are achieved by combining trails discovered on several graphs, where each graph corresponds to interactions in one of five different coupling types (Inheritance, Interface, Aggregation, Parameter Type and Return Type) [40]. In these examples, the problems identified earlier are largely eliminated and the true potential of the trail-based navigation engine can be clearly seen. The navigation problem is widespread and occurs in all type of software systems. Alan Cooper describes the phenomenon as “uninformed consent”, when “at each
step the user is required to make a choice, the scope and consequences of which are not known” [13]. Providing keyword search and trail discovery over the graph of options available at the application or operating system level could greatly enhance user experience. For example in Microsoft Windows, the query “active desktop” might return a path Start → Settings → Control Panel → Folder Options. Finally, we believe that the algorithm may have applications in the fields of game playing and optimization problems.

8. REFERENCES

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