Assessing the effect of geographically correlated failures on interconnected power-communication networks

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Assessing the Effect of Geographically Correlated Failures on Interconnected Power-Communication Networks

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Abstract—We study the reliability of power transmission networks under regional disasters. Initially, we quantify the effect of large-scale non-targeted disasters and their resulting cascade effects on power networks. We then model the dependence of data networks on the power systems and consider network reliability in this dependent network setting. Our novel approach provides a promising new direction for modeling and designing networks to lessen the effects of geographical disasters.

I. INTRODUCTION

Power transmission networks are vulnerable to large-scale natural disasters, such as hurricanes or geomagnetic storms [1], [7], [13]. The geographical layout of the network affects the impact of such real-world disasters since they occur in specific geographic locations. For example, an Electromagnetic Pulse (EMP) attack [10] or geomagnetic storm can cause failure of electric power lines that directly transmit power to a large city, thereby likely causing significant disruptions to power services. However, the damage to the power network infrastructure is not necessarily limited to these initial failures; power networks are also vulnerable to cascading failures. Cascading failures occur when an initial failure in the network changes power flows, which must obey physical law constraints, such that additional lines overload and fail. This in turn causes the power flows to change again; this process will continue until some stability is reached. A well known example of a cascading failure is the 2003 blackout where a significant area of the northeastern U.S. lost power [2]. In this paper we consider two failure models. The first model considers power networks with respect to a randomly located geographic disaster and subsequent cascading failures. The second model builds on the first; we describe a dependency between power and data networks and consider the connectivity of data networks in this context. For each model, we present numerical results based on real-world networks.

II. OVERVIEW OF MODELS AND RELATED WORK

Motivated by the effects of natural disasters and cascading failures, we initially consider a two-stage failure model for power networks. The first stage removes power lines that intersect a randomly located disk (which models a geographically correlated failure). The second stage then calculates the cascading failure that occurs due to the removal of the initial links. By using the tools developed in our previous work [11] and the cascading failure model presented in [5], we are able to calculate the effect of this type of failure in power networks.

To the best of our knowledge, [4] is the only other work to look at the effect of geographically correlated failures on power networks.

Next, motivated by the effects of power loss on data networks [9], we consider the survivability of data networks with respect to power networks. We assume data nodes rely on the operation of the closest power load nodes in order to function. We present numerical results that show data network connectivity is significantly lower when power network dependency is considered; this implies power network effects have a significant impact on the survivability of real-world data networks.

Power network resilience has been considered in the past [3], [6], however so far only [4] has considered the effects of a targeted geographic failure model. In this work we consider the effect of non-targeted geographic disasters on the power network. Some recent work has modeled the interdependence between data and power networks and demonstrated asymptotic percolation results [8]; however they did not consider power flows or geography in their models. Additionally, [14] considered a geographic dependence model but did not consider failures which were geographically correlated.

III. ASSESSING POWER NETWORK RELIABILITY

We now consider a geographic failure model for power networks where a disaster is modeled as a ‘randomly’ located disk. This can describe the effect of some natural disasters such as geomagnetic storms [1], [7], [13] or hurricanes, in addition to collateral (non-targeted) damage from attacks on other continental networks (e.g. an attack on the communication or transportation networks). Our goal is to be able to understand and quantify the effect of large-scale non-targeted disasters and their resulting cascade effects on the power network. We first describe the network and failure model and then propose metrics to be evaluated on a real-world network.

A. Network and Failure Model

We consider a network such that nodes are represented by points on the plane and links are represented by line segments. This is the same model used in previous and related work [4], [11].

The failure model consists of two stages; the first stage is link failures caused by the random circular disaster and the next stage is the resulting cascading failures. We first describe
the initial failures caused by the random circular disk (which is the same as the failure model presented in [11]). We model a disaster event in the network as a single randomly located disk of a radius \( r_b \) centered within an area of interest \( C \) (i.e. \( C \) is a set of points in the plane where the disaster may be centered). If the randomly located disk intersects some power lines, we assume those lines are destroyed.

Geometric probability [16] allows us to assign a measure to sets of disks. This measure is simply defined as the Lebesgue integral over the set of disk centers. Using this measure and tools from computational geometry, we can find the probability that a randomly located disk centered in \( C \) intersects only \( l_3 \) and \( l_4 \) is given by the ratio of the area of the shaded region to the area of the large rounded rectangle.

After this initial failure, due to power flow constraints, a cascading failure may occur. We will use the same power flow and cascading failure model described in [5]. Thus these geometric probability tools along with the cascading failure model allow us to analyze the effects of large scale randomly located disasters on the power network.

We now present our failure model for power flows and cascading failures in power networks. We use the same models as found in [4], [5] and even borrow some notation. The details of the DC power flow and cascading model may be skipped and the reader may proceed to Section III-B without loss of continuity.

1) DC Power Flow Model: We now describe the DC power flow model which is a linearized version of the more complicated AC power flow model. We use the DC model because it is more tractable and easier to find solutions for power flows.

Let \( \beta_i \) represent the amount of power injected at node \( i \). If \( \beta_i > 0 \) then node \( i \) is a source of power and may represent a generator where power is injected into the system. If \( \beta_i < 0 \) then node \( i \) is a sink of power and may represent demand at this node. We call these type of nodes power demand nodes. If \( \beta_i = 0 \) then power is neither injected or removed at node \( i \) and may represent a power bus. Let \( N \) be the set of nodes in the network.

Let \( (i, j) \) denote the power line from node \( i \) to node \( j \) and let \( E \) denote the set of all these lines. Let \( x_{ij} \) denote the reactance of \( (i, j) \) and let \( u_{ij} \) denote the capacity of \( (i, j) \).

A DC power flow can be described by the amount of power to flow from node \( i \) to node \( j \) on \( (i, j) \), denoted by \( f_{ij} \), and the phase angle at node \( i \), denoted by \( \theta_i \). A DC power flow must obey the following constraints.

\[
\sum_{j : (i, j) \in E} f_{ij} = \beta_i \quad \forall i \in N \tag{1}
\]

\[
\theta_i - \theta_j = x_{ij} f_{ij} \quad \forall (i, j) \tag{2}
\]

Equation (1) constrains the total power out of a node to be equal to the amount of power injected at that node (power conservation). For example, if a node is a generator then the net power flow out must be the amount of power generated at that node. Equation (2) is the analogue to Ohm’s law; the amount of power through a power line is proportional to the difference in phase angles \( \theta_i \) and \( \theta_j \).

It should be noted that the power flow has a feasible solution as long as \( \sum_{i \in K} \beta_i = 0 \) for every connected component \( K \) in the network (that is, aggregate supply equals aggregate demand for that component) [5]. Additionally, the values of the power flows are unique [5].

2) Cascading Failure Model: We now describe the cascading failure model. Again, this model can be found in [4], [5], but is presented here for completeness.

Before any failures occur, we assume the network is connected and that \( \sum_{i \in N} \beta_i = 0 \). In other words, we assume aggregate demand is equal to aggregate supply.

We now describe the cascading failure model in steps.

1) Set \( \tilde{f}_{ij} \) to be the absolute value of the power flow on \((i, j)\) before any failure occurs.
2) Consider some subset of power lines to be initially removed from the network.
3) In order to calculate DC power flows for this modified network, aggregate supply and demand must match in each component. Hence, we proportionately reduce supply (or demand) at nodes in each component until this condition is met. This may model load shedding or a ramping down of generators.
4) Power flows $f_{ij}$ are then calculated for the remaining network by finding the unique power flows that satisfy equations 1 and 2.
5) Let $\tilde{f}_{ij} = \alpha |f_{ij}| + (1-\alpha)f_{ij}$. $\tilde{f}_{ij}$ represents some ‘moving average’ of flow through the power line $(i,j)$ and can be thought of as modeling the effect of some thermal effects. $\alpha$ is a parameter in this moving average set to a value between 0 and 1. If $\alpha$ is small, then the line will take more time steps to ‘heat up’; if $\alpha = 1$ then the line can be thought of as feeling the effect of the new flow instantaneously. In this work we assume $\alpha = 0.5$.
6) We then remove all lines for which $\tilde{f}_{ij} > u_{ij}$. This may cause an additional change in the power flows (hence the cascade); we go back to step 3 and the process repeats until no flow is above capacity.

It should be noted that we were not able to attain the capacities of power lines for real power networks. Hence, in order to approximate the capacities on a power network we calculate the initial power flows on each line and then set $u_{ij}$ proportional to $|f_{ij}|$ before any failures occur. This proportion is called the Factor of Safety (FoS) and relates to the amount of ‘spare capacity’ on the power lines. In other words $u_{ij} = |f_{ij}| \times FoS$ before any failures occur. For real power grids, it is believed that a good approximation for FoS is 1.2 [4]. Hence, for the majority of this work, we assume FoS = 1.2.

B. Performance Metrics and Numerical Results

Our goal is to analyze the effect of a randomly located circular disk failure in conjunction with cascading failures on power networks. Let the yield be the fraction of demand satisfied after the disaster and resulting cascade. By calculating the probabilities of relevant joint link failures using the tools and equations in [11] and considering the resulting cascading effects, one can evaluate the expected value as well as the distribution of the yield to a randomly located disk failure event.

We now discuss some numerical results based on the HVIEET network¹. Fig. 3 shows the cumulative distribution function (CDF) of the average yield on the HVIEET network with disaster radius of 50 kilometers. Addressing the effect of Factor of Safety, Fig. 4 shows how average yield changes as the factor of safety (FoS) is changed (Factor of Safety relates to the amount of ‘spare capacity’ on power lines). Note when FoS = 1, then there is no spare capacity allocated on the power lines, so when a failure event occurs the resulting cascading failure brings down most of the network. As FoS increases, the amount of spare capacity on the power lines increase, so the average yield increases as well, as one would expect. For example, when FoS = 2 the failure event will not have much effect on the yield. Addressing the effect of the radius of the disaster, Fig. 5 shows as the radius of the initial disaster increases, the average yield in the network decreases.

We now compare the effect of independent random link failures to the effect of a randomly located circular failure. We initially calculate the average yield of HVIEET to a circular disaster while the size of the region of interest $C$ varies. The size of $C$ is varied to change the probability a unit of fiber is cut. So we can plot average yield versus the probability a unit of fiber is cut. See Fig. 6 for results.

Next, we calculate average yield assuming independent link failures such that links fail with the same probability as in the random disk-cut case. Thus the probability a link fails is still a function of its length, however links fail independently. Since the total number of power lines is not small, calculating average yield by enumerating all possible failures is not feasible (possible failures are exponential in number of links). Instead we use a Monte Carlo approach, using 4000 samples

¹We would like to thank the authors of [14], [15] for sharing their data.
geographic disasters on power networks have key differences than in the case of random disk-cuts. This result demonstrates from independent smaller scale failures (e.g. power line failure for each particular probability of unit link failure samplepoint. As in the random disk case. Fig. 5. Average yield vs. radius (in terms of degrees of latitude/longitude) on the HVIET network. As the radius of the initial disaster increases, the average yield in the network decreases.

![Average Yield vs. Probability of Unit Link Failure](image)

Fig. 6. The solid line shows average yield in HVIET versus the probability a unit (latitude/longitude) of power line is cut by a random disk of radius approximately 8km. The dashed line shows average yield in HVIET assuming power lines fail independently such that lines fail with the same probability as in the random disk case. For each particular probability of unit link failure sample point. See Fig. 6 for results.

Notice that average yield under independent failures is less than in the case of random disk-cuts. This result demonstrates geographic disasters on power networks have key differences from independent smaller scale failures (e.g. power line failure due to brush growth). Perhaps this is because some power supply nodes and power demand nodes are near each other and so a random disk may be more likely to effectively remove both these nodes simultaneously which may reduce the chances of a large cascading failure (since power loads will remain balanced). Also note the contrast to the result in [11] for the NSFNET data network where independent failures on a data network have less impact than in the case of random disk-cuts; this highlights a fundamental difference in the survivability between power and data networks.

C. Possible Extensions

In the context of random geographic failures and power networks, the following problems are potential extensions for future work.

Other metrics: Consider other metrics beyond yield such as the distribution of number of lines destroyed or the distribution of connected components. These distributions will allow us to better understand the impact of a random geographical disaster on the survivability of the power grid.

Computationally efficient algorithms: Development of efficient algorithms to calculate the yield in general networks that scale well with network size. Analyzing the running time of our current algorithms and developing faster methods will allow us to obtain numerical results on larger and more detailed real-world power networks.

Extending the probabilistic failure model: Currently, our model assumes that every power line intersected by a circular disk is removed from the network. However, power lines within a disaster region may not always fail (e.g. shielded power lines near a hurricane may remain operational). So the disaster may have a probabilistic effect on the lines. It would be interesting to capture this doubly random effect; we model a disaster as a randomly located disk that also has a non-deterministic effect on the intersected power lines.

AC Power Flow Model: A more realistic power flow model can be considered. Currently, many papers on power networks assumes a DC power flow model [6] [4]; this type of model is very simple and ignores certain effects that may occur during a cascade. The AC power flow model is a more realistic flow model, though it is harder to solve for the flow equations [12]. We can alter our failure model to incorporate the more realistic AC power flow model and study the impact of the cascading model on yield and other performance metrics.

Robust Design: In addition to the above items, we can study some power network design issues. One goal may be to increase the average yield in the network under a random circular disk disaster. To this end, we may consider how to add additional power lines or increase capacities of certain power lines in order to increase average yield. For example, we may consider what Factor of Safety is required to guarantee the expected yield above a certain threshold.

IV. RELIABILITY OF DEPENDENT NETWORKS

Many systems and networks depend on reliable delivery of power from the electric grid. For example, power is required to operate street lights for transportation networks in cities. Another example are fiber networks; power is needed at backbone routers and amplifiers (on fiber links) or else those components will fail. Since cascading power outages can be widespread, their effect on dependent systems can be devastating. In particular, due to the widespread nature of blackouts, continental fiber networks may become disconnected if the power failure affects a large area that includes the networks physical components. For example, the blackouts of 2003 had a significant effect on the connectivity of the Internet [9].

Motivated by the dependencies of many networks and systems on the power network, we consider the design of robust infrastructures with respect to cascading power failures caused by a randomly located geographic disaster. We first describe a model for the dependence of a network on the power network. We then present our failure model and compare data network reliability with and without power network dependency.
A. Dependence on Power Network

As described above, many networks and systems require power to operate properly; that is, failure to provide power to systems can cause failure in those dependent systems. Although these systems typically have backup power supplies, backup generators are often unreliable. We assume, as in the previous section, that the power network is represented by points and line segments in the plane. Similarly, we assume the dependent network is also modeled by points and line segments. A dependent node is likely to draw its power from a nearby substation. So, we let a dependent node be operational when a demand node fails, data nodes located within its Voronoi cell are assumed to fail as well.

B. Failure Model

We use the same failure model for the power grid presented in the previous section augmented with data-power network dependency. This failure model consists of three stages; the first stage is link failures caused by the random circular disaster and the next stage is the resulting cascading failures in the power network. Then, the effects on the dependent network (based on geographical proximity to supply nodes) are considered once the cascading failures have occurred.

C. Metrics for Dependent Network Robustness

Our goal is to assess the reliability of networks to failures in the power grid. In the context of a random geographic failure on the power grid and the resulting impact on dependent networks, we propose to consider the following metrics:

- Connectivity - In many networks, especially data networks, we are concerned with connectivity; i.e. does the network remain connected. For example, we would like for all major U.S. cities to be able to communicate with each other, therefore it is reasonable to consider the connectivity of the continental fiber network. Thus, we can consider the probability that the dependent network remains connected after a randomly located disaster on the power grid.

- ATTR - If a connected network cannot be guaranteed after a failure or full connectivity is not critically important, it may be useful to consider the ATTR metric. This is given by the probability a randomly chosen pair of nodes in the dependent network remain connected after a randomly located disaster on the power grid. In the following, we consider the effect of random disasters on real-world dependent networks using this metric.

D. Numerical Results

Using the failure model just described, we present some numerical results based on the Italian research network (GARR) and the Italian high-voltage electrical transmission network (HVIET) [14],[15]. Consider Fig. 8. Via a Monte Carlo simulation, this figure shows how ATTR for the Italian research network (GARR) as a function of the radius (in latitude/longitude coordinates) of a randomly located circular disaster when no power networks are considered (using tools and models from [11]). The blue solid curve shows ATTR for the GARR network when the dependency effects of Italian high-voltage electrical transmission network (HVIET) are considered. For every radius considered a Monte Carlo approach with 4000 samples was used. We note that ATTR is significantly lower when power network dependency is considered; this implies power network effects have a significant impact on the survivability of real-world data networks.

E. Possible Extensions

In the context of a random geographic disaster on the power grid and its effect on dependent networks, one can consider to study some network design problems. One goal may be to increase the connectivity or ATTR metric in the dependent network. To this end, we may consider how to add additional power lines or increase capacities of certain power lines in
Motivated by the effects of natural disasters such as geomagnetic storms [13] and cascading failures, in this paper we considered a two-stage failure model for power networks. The first stage removes power lines that intersect a randomly located disk and the second stage calculates the cascading failure that occurs due to the removal of the initial links. We used the tools developed for randomly located circular cuts and a cascading failure model to calculate the effect of this type of failure in power networks. Then motivated by the effects of power loss on data networks [9], we considered the survivability of data networks with respect to power networks. We assumed data nodes rely on the operation of the closest power demand nodes to function. Through numerical results, we were able to show power network effects have a significant impact on the survivability of real-world data networks. Our novel approach provides a promising new direction for modeling and designing networks to lessen the effects of geographical disasters.

VI. ACKNOWLEDGEMENTS

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