An alternative text representation
to TF-IDF and Bag-of-Words *

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ABSTRACT
In text mining, information retrieval, and machine learning, text documents are commonly represented through variants of sparse Bag of Words (sBoW) vectors (e.g. TF-IDF [1]). Although simple and intuitive, sBoW style representations suffer from their inherent over-sparsity and fail to capture word-level synonymy and polysemy. Especially when labeled data is limited (e.g. in document classification), or the text documents are short (e.g. emails or abstracts), many features are rarely observed within the training corpus. This leads to overfitting and reduced generalization accuracy. In this paper we propose Dense Cohort of Terms (dCoT), an unsupervised algorithm to learn improved sBoW document features. dCoT explicitly models absent words by removing and reconstructing random sub-sets of words in the unlabeled corpus. With this approach, dCoT learns to reconstruct frequent words from co-occurring infrequent words and maps the high dimensional sparse sBoW vectors into a low-dimensional dense representation. We show that the feature removal can be marginalized out and that the reconstruction can be solved for in closed-form. We demonstrate empirically, on several benchmark datasets, that dCoT features significantly improve the classification accuracy across several document classification tasks.

* A modified version of our CIKM 2012 paper: From sBoW to dCoT, Marginalized Encoders for Text Representation

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1. INTRODUCTION
The feature representation of text documents plays a critical role in many applications of data-mining and information retrieval. The sparse Bag of Words (sBoW) representation is arguably one of the most commonly used and effective approaches. Each document is represented by a high dimensional sparse vector, where each dimension corresponds to the term frequency of a unique word within a dictionary or hash-table [2]. A natural extension is TF-IDF [1], where the term frequency counts are discounted by the inverse-document-frequencies. Despite its widespread use with text and image data [3], sBoW does have some severe limitations, mainly due to its often excessive sparsity.

Although the Oxford English Dictionary contains approximately 600,000 unique words, it is fair to say that the essence of most written text can be expressed with a far smaller vocabulary (e.g. 5000–10000 unique words). For example the words splendid, spectacular, terrific, glorious, resplendent are all to some degree synonymous with the word good. However, as sBoW does not capture synonymy, a document that uses “splendid” will be considered dissimilar from a document that uses the word “terrific”. A classifier, trained to predict the sentiment of a document, would have to be exposed to a very large set of labeled examples to learn that all these words are predictive towards a positive sentiment.

In this paper, we propose a novel feature learning algorithm that directly addresses the problems of excessive spar-
say that their approach is computationally most demanding. Similarly to LSI, pLSI and LDA, our algorithm also maps the sparse sBoW features into a low dimensional dense representation. However it is faster to train and addresses the problem of synonymy more explicitly.

3. dCoT

First, we introduce notations that will be throughout the paper. Let $D = \{w_1, \ldots, w_d\}$ be the dictionary of words that appear in the text corpus, with size $d = |D|$. Each input document is represented as a vector $x \in \mathbb{R}^d$, where each dimension $x_i$ counts the appearance of word $w_i$ in this document. Let $X = [x_1, \ldots, x_n]$ denote the corpus. Assume that the first $n_t \ll n$ documents are accompanied by corresponding labels $\{y_1, \ldots, y_{n_t}\} \in Y$, drawn from some joint distribution $D$.

In this section we introduce the algorithm dCoT, which translates sparse sBoW vectors $x \in \mathbb{R}^d$ to denser and lower dimensional prototype vectors. We first define the concept of prototype terms and then derive the algorithm step-by-step.

Prototype features. Let $P = \{w_{p_1}, \ldots, w_{p_r}\} \subset D$, with $|P| = r$ and $r < d$, denote a strict subset of the vocabulary $D$, which we refer to as prototype terms. Our algorithm aims to "translate" each term in $D$ into one or more of these prototype words with similar meaning. Several choices are possible to identify $P$, but a typical heuristic is to pick the $r$ most frequent terms in $D$. The most frequent terms can be thought of as representative expressions for sets of synonyms — e.g. the frequent word good represents the rare words splendid, spectacular, terrific, glorious. For this choice of $P$, dCoT translates rare words into frequent words.

Corruption. The goal of dCoT is to learn a mapping $W : \mathbb{R}^d \rightarrow \mathbb{R}^r$, which "translates" the original sBoW vectors in $\mathbb{R}^d$ into a combination of prototype terms in $\mathbb{R}^r$. Our training of $W$ is based on one crucial insight: If a prototype term already exists in some input $x$, $W$ should be able to predict it from the remaining terms in $x$. We therefore artificially create a supervised dataset from unlabeled data by removing (i.e. setting to zero) each term in $x$ with some probability $(1 - p)$. We perform this $m$ times and refer to the resulting corrupted vectors as $x^1, \ldots, x^m$. We not only remove prototype features but all features, to generate more diverse input samples. (In the subsequent section we will show that in fact we never actually have to create this corrupted dataset, as its creation can be marginalized out entirely — but for now let us pretend it actually exists.)

Reconstruction. In addition to the corruptions, for each input $x_i$ we create a sub-vector $\bar{x}_i = [x_{p_1}, \ldots, x_{p_r}] \in \mathbb{R}^r$ which only contains its prototype features. A mapping $W \in \mathbb{R}^{r \times d}$ is then learned to reconstruct the prototype features from the corrupted version $\hat{x}_i$, by minimizing the squared reconstruction error,

$$\frac{1}{2hn} \sum_{i=1}^{n} \sum_{j=1}^{m} ||\bar{x}_i - W\bar{x}_i||^2.$$ (1)

To simplify notation, we assume that a constant feature is added to the corrupted feature, $\hat{x}_i = [\bar{x}_i; 1]$, and an appropriate bias is incorporated within the mapping $W = [W, b]$. Note that the constant feature is never corrupted. The bias term has the important task of reconstructing the average occurrence of the prototype features.
Let us define a design matrix
\[ \tilde{X} = [\tilde{x}_1, \cdots, \tilde{x}_m, \cdots, \tilde{x}_n] \in \mathbb{R}^{r \times n \times m} \]
as the \( m \) copies of the prototype features of the inputs. Similarly, we denote the \( m \) corruptions of the original inputs as
\[ \tilde{X} = [\tilde{x}_1, \cdots, \tilde{x}_m, \cdots, \tilde{x}_n] \in \mathbb{R}^{d \times n \times m}. \]
With this notation, the loss in eq. (1) reduces to
\[
\frac{1}{2nm} \| \tilde{X} - W \tilde{X} \|_F^2, \tag{2}
\]
where \( \| \cdot \|_F \) denotes the squared Frobenius norm. The solution to (2) can be obtained under closed-form as the solution to the well-known ordinary least square.

Marginalized corruption. Ideally, we would like the number of corrupted versions become very large, i.e. \( m \to \infty \). By the weak law of large numbers, \( \mathbf{R} \) and \( \mathbf{Q} \) then converge to their expectations and (3) becomes
\[
W = E[\mathbf{R}][E[\mathbf{Q}])^{-1}, \tag{4}
\]
with the expectations of \( \mathbf{R} \) and \( \mathbf{Q} \) defined as
\[
E[\mathbf{Q}] = \frac{1}{n} \sum_{i=1}^{n} E[\hat{x}_i \bar{\hat{x}}_i^T], \quad E[\mathbf{R}] = \frac{1}{n} \sum_{i=1}^{n} E[\bar{x}_i \bar{\hat{x}}_i^T]. \tag{5}
\]
The uniform corruption allows us to compute the expectations in (3) in closed form. Let us define a vector \( q = [q_1, \ldots, q_p, 1] \in \mathbb{R}^{d+1} \), where \( q_0 \) indicates if feature \( \alpha \) survive a corruption (the constant feature is never corrupted, hence \( q_{d+1} = 1 \)). If we denote the scatter matrix of the uncorrupted input as \( S = XX^T \), we obtain \( E[\mathbf{R}]_{\alpha \beta} = S_{\alpha \beta} q_\alpha \) and
\[
E[\mathbf{Q}]_{\alpha \beta} = \begin{cases} S_{\alpha \beta} q_\alpha q_\beta & \text{if } \alpha \neq \beta \\ S_{\alpha \beta} q_\alpha & \text{if } \alpha = \beta. \end{cases} \tag{6}
\]
The diagonal entries of \( E[\mathbf{Q}] \) are the product of two identical features, and the probability of a feature surviving corruption is \( p \). The expected value of the diagonal entries is therefore the scatter matrix multiplied by \( p \). The off-diagonal entries are the product of two different features \( \alpha \) and \( \beta \), which are corrupted independently. The probability of both features surviving the corruption is \( p^2 \).

Squashing function. The output of the linear mapping \( W : \mathbb{R}^d \to \mathbb{R}^r \) approximates the expected value (4) of a prototype term. It can be beneficial to have more bag-of-word like features that are either present or not. For this purpose, we apply the tanh() squashing-function to the output
\[
z = \tanh(Wx), \tag{7}
\]
which has the effect of amplifying or dampening the feature values of the reconstructed prototype words. We refer to our feature learning algorithm as dCoT (Dense Cohort of Terms).

3.1 Recursive re-application

The linear mapping in eq. (4) is trained by reconstructing prototype words from partially corrupted input vectors. This linear approach works well for prototype words that commonly appear together with words of similar meaning (e.g. “president” and “obama”), as the mapping captures the correlation between the two. It can however be the case that two synonyms never appear together because the input documents are short and the authors use one term or the other but barely both together (e.g. “tasty” and its rarer synonym “delicious”). In these cases it can help to recursively re-apply dCoT to its own output. Here, the first mapping reconstructs the context of the input, which is the context between synonyms (i.e. words that co-occur with all synonyms) and subsequent applications of dCoT reconstruct the synonym-prototypes from this context. In the previous example, one could imagine that the first application of dCoT constructs context prototype words like “food”, “expensive”, “dinner”, “wonderful” from the original term “delicious”. The re-application of dCoT constructs “tasty” from these context words.

Let the mapping from eq. (4) be \( W^1 \in \mathbb{R}^{r \times d} \) and \( \tilde{z}_i = \tanh(W^1 x_i) \) for an input \( x_i \). We now compute a second mapping \( W^2 \in \mathbb{R}^{r' \times r} \), exactly as defined in the previous section, except that we consider the vectors \( \tilde{z}_1, \ldots, \tilde{z}_n \in \mathbb{R}^r \) as input. The mapping \( W^2 \) is an affine transformation which stays within the prototype space spanned by \( P \). This process can be repeated many times and because the input dimensionality is low the computation of (4) is cheap. Figure 1 illustrates this process in a schematic layout.

If dCoT is applied \( l \) times, the final representation \( z_l \) is the concatenated vector of all outputs and the original input,
\[
z_l = (x_i, \tilde{z}_1, \cdots, \tilde{z}_n)^T. \tag{8}
\]

4. CONNECTION

dCoT shares some common elements with previously proposed feature learning algorithms. In this section, we discuss their similarities and differences.

Stacked Denoising Autoencoder (SDA). In the field of image recognition, the Autoencoder [15] and the Stacked Denoising Autoencoder (SDA) [19] are widely used to learn better feature representation from raw pixels input. dCoT shares several core similarities with SDA, which in fact inspired its original development. Similar to dCoT, SDA first corrupts the raw input, and learns to re-construct it. SDA also stacks several layers together by feeding the output of previous layers as input into sub-sequent layers. However,
the two algorithms also have substantial differences. The mapping in dCoT is a linear mapping from input to output (with a sub-sequent application of tanh()), which is solved in closed form. In contrast, SDA employs non-linear mapping from the input to a hidden layer and then to the output. Instead of a closed-form solution, it requires extensive gradient-descent-type hill-climbing. Further, SDA actually corrupts the input and is trained with multiple epochs over the dataset, whereas dCoT marginalizes out the corruption. In terms of running time, dCoT is orders of magnitude faster than SDA and scales to much higher dimensional inputs.

Principle Component Analysis (PCA). Similar to dCoT, Principle Component Analysis (PCA) learns a lower dimensional linear space by minimizing the reconstruction error of the original input. For text documents, PCA is widely known through its variant as latent semantic indexing (LSI) [5]. Although both dCoT and LSI minimize reconstruction errors, the exact optimization is quite different. dCoT explicitly reconstructs prototype words from corruption, whereas LSI minimizes the reconstruction error after dimensionality reduction.

5. RESULTS

We evaluate our algorithm on Reuters and Dmoz datasets together with several other algorithms for feature learning.

Datasets. The Reuters-21578 dataset is a collection of documents that appeared on Reuters newswire in 1987. We follow the convention of [23], which removes documents with multiple category labels. The dataset contains 65 categories, and consists of 5946 training and 2347 testing documents. Each document is represented by sBoW representation with 18933 distinct terms. The dataset contains 65 categories, the dataset consists of 16 categories. Following the convention of [24], we labeled each input by its top-level category, and remove some low-frequent terms. As a result, the dataset contains 7184 and 1796 training and testing points respectively, and each input is represented by the sBoW representation that contains 16498 distinct terms.

Reconstruction. Figure 2 shows example input terms (essentially one-word documents) and the prototype words that are reconstructed with dCoT on the Reuters dataset.

Each column represents a different input term (e.g. a document consisting of only the term “nasdaq”) and shows the reconstructed prototype terms in decreasing order of their feature values (top to bottom). The very left column shows the prototype terms generated by an all-empty input document.

Figure 2: Term reconstruction from the Reuters dataset. Each column shows a different input term (e.g. “reagan”, “nasdaq”), along with the prototype terms reconstructed from this particular input in decreasing order of feature values (top to bottom). The very left column shows the prototype terms generated by an all-empty input document.

Figure 3: Classification accuracy trend on Reuters dataset with different layers and noise levels.

Each column represents a different input term (e.g. a document consisting of only the term “nasdaq”) and shows the reconstructed prototype terms in decreasing order of their feature values (top to bottom). The very left column shows the prototype features generated by an all-empty input document. These features are completely determined by the constant bias, and coincide with the most frequent prototype terms in the whole corpora. For all other columns, we subtract this bias-generated vector to highlight the prototype words generated by the actual word and not the bias. As shown in the figure, two trends can be observed. First, prototype terms are reconstructed by other less common and more specific terms. For example, president is reconstructed by reagan and bush, and stock is reconstructed by nasdaq. Both reagan and bush are specific terms describing president. This trend indicates that dCoT learns the mapping from rare terms to common terms. Second, context and topics are reconstructed from rarer terms through the recursive re-application. For example, agriculture is reconstructed by reproduction, indicating that documents containing reproduction typically discuss topics related to agriculture. This connection indicates that dCoT also learns the higher order correlations between terms and topics.

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Parameter sensitivity. We also evaluate the effect of different noise level and number of layers (i.e. the number of recursive re-applications). Figure 3 shows the classification results on Reuters dataset as a function of layers $l$ and noise level $1 - p$. After training of dCoT (on the whole dataset), we randomly select 1,000 labeled training inputs, train an SVM classifier [17] on the new feature representation, and test on the full testing set. Two trends emerge: 1. deep layers $l > 1$ improve over a single layered transformation — supporting our hypothesis that as we recursively re-apply dCoT, not only the feature representation is enriched, but also the higher order correlations between terms and topics are learned. 2. best results are obtained with a surprisingly high level of noise. We explain this trend by the fact that more corruption helps discover more subtle relationships between features and as we operate in the limit, and integrate out all possible corruptions, we can still learn even from substantially shortened documents.

Semi-supervised Experiments. In many real-world applications, the labeled training inputs are limited, because labeling usually involves human interaction and is expensive and time-consuming. However, unlabeled data is usually large and available. In this experiment we evaluate the suitability of dCoT to take advantage of semi-supervised learning settings. We learn the new feature representation with dCoT on the full training set (without labels), but train a linear SVM classifier on a small subset of labeled examples. We gradually increase the size of the labeled subset and evaluate on the whole testing set. For any given number of labeled training inputs, we average over five runs (of randomly picked labeled examples). We use the validation set to select the best combination of noise level and the number of layers.

As baselines, we compare against several alternative feature representations, which are all obtained from the full training set, similarly applied to a linear SVM classifier. The most basic baselines are the sBoW representation (with term frequency counts) and TF-IDF [1]. We compute the TF for each document separately, and obtain the IDF from the whole training set (including labeled and unlabeled data). We then apply the same IDF to the testing set. We also compare against latent semantic indexing (LSI) [5], for which we further split the training set into training and validation. We use the validation set to find the best parameter (numbers of leading Eigenvectors), and retrain on the whole training set with the best parameter. The new representation is obtained by projecting the sBoW feature space onto the LSI eigenvectors. Finally, we also compare against Latent Dirichlet Allocation (LDA) [4]. Similar to LSI, we use a validation set to find the best parameters, which include the Dirichlet hyper-parameter and the number of topics. The new representation learned from LDA are the topic mixture probabilities.

The classification results are presented in figure 4. The graph shows that on both Dmoz and Reuters datasets, dCoT generally out-performs all other algorithms. This trend is particularly prominent in settings with relatively little labeled training data.

Running time. Table 1 compares the running times for feature learning with different algorithms. All timings are performed on a desktop with dual Intel® Six Core Xeon X5650 2.66GHz processors. Compared to LDA and LSI, the timing results show a three orders of magnitude speed-up on two datasets, reducing the feature learning time from several hours to a few minutes.

| Datasets | TF-IDF | LSI | LDA | dCoT |
|----------|--------|-----|-----|------|
| Reuters  | 1s     | 51m| 3h10m| 2m   |
| Dmoz     | 1s     | 1h38m| 9h1m| 3m   |

Table 1: Running time required for unsupervised feature learning with different algorithms.

6. CONCLUSION

In this paper we present dCoT, an algorithm that efficiently learns a better feature representation for sBoW document data. Specifically, dCoT learns a mapping from high dimensional sparse to low dimensional dense representations by translating rare to common terms. Recursive re-application of dCoT on its own output results in the discovery of higher order topics from raw terms. On two standard benchmark document classification datasets we demonstrate that our algorithm achieves state-of-the-art results with very high reliability in semi-supervised settings.
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