SARS-COV-2: SIR Model Limitations and Predictive Constraints

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Abstract: Background: The main purpose of this research is to describe the mathematical asymmetric patterns of susceptible, infectious, or recovered (SIR) model equation application in the light of coronavirus disease 2019 (COVID-19) skewness patterns worldwide. Methods: The research modeled severe acute respiratory syndrome coronavirus 2 (SARS-COV-2) spreading and dissemination patterns sensitivity by redesigning time series data extraction of daily new cases in terms of deviation consistency concerning variables that sustain COVID-19 transmission. The approach opened a new scenario where seasonality forcing behavior was introduced to understand SARS-COV-2 non-linear dynamics due to heterogeneity and confounding epidemics scenarios. Results: The main research results are the elucidation of three birth- and death-forced seasonality persistence phases that can explain COVID-19 skew patterns worldwide. They are presented in the following order: (1) the environmental variables (Earth seasons and atmospheric conditions); (2) health policies and adult learning education (HPALE) interventions; (3) urban spaces (local indoor and outdoor spaces for transit and social-cultural interactions, public or private, with natural physical features (river, lake, terrain). Conclusions: Three forced seasonality phases (positive to negative skew) phases were pointed out as a theoretical framework to explain uncertainty found in the predictive SIR model equations that might diverge in outcomes expected to express the disease’s behaviour.

Keywords: COVID-19 seasonality; S.I.R. models; mathematical modeling; forced seasonality; confounding variables; uncertainty

1. Introduction

This research’s main focus is to point, as noted in Grassly and Fraser [1], to the consequences of seasonality for endemic $R_0$ stability in order to understand and obtain an endemic equilibrium for coronavirus disease 2019 (COVID-19) involving mixing patterns such as environmental driving factors, policy interventions, and urban spaces [2–8]. These latter three variables might pose challenges for the outcomes of the SIR (susceptible, infectious, or recovered) predictive analysis [9] of severe acute respiratory syndrome coronavirus 2 (SARS-COV-2) spreading and dissemination patterns. This can be verified in the time series data regarding daily new COVID-19 cases where the type of spreading patterns in daily quantitative outcomes present a high degree of uncertainty (skewness asymmetric patterns) expressed by fluctuations and mainly random distributions [8].

By observing time series data of daily new COVID-19 cases worldwide [10], the epidemics birth and death persistence present different probabilistic distributions for each sample (country) of observation, with many delays and fluctuations for the outbreak, peak and control phases due to no initial predefined conditions within the overall samples (countries). These data with distinct outcomes among countries originate false phenomenon observations in terms of positive and negative skew to allow predictive analysis based on SIR models and derivations [11]. This is due to these models relying upon a predefined type of health policies interventions, pre-assumed human behavior and predefined spatial or temporal analysis towards outbreaks, peak and control phases. These pre-assumptions
were investigated theoretically although stability to instability patterns generated by the variables that sustain the disease occurrence.

The research divided data of daily new COVID-19 cases into three phases of forced seasonality, demonstrated by a mathematical model of skewness presented in the phenomenon derived from a brief topological analysis and the confounding variables that sustain the disease transmission. Consequently, it suggests specific data extraction from time series in order to make predictive analysis with SIR models. This approach aims to provide a more robust understanding of the scientific results concerning these topics of study and worldwide strategies to reduce SARS-COV-2 dissemination patterns of daily new COVID-19 cases to control infection spreading and dissemination patterns. The three main birth and death seasonality persistence (ε') phases found in this research are in the following order: (1) the environmental variables (Earth seasons and atmospheric conditions); (2) health policies and adult learning education (HPALE) interventions; (3) urban spaces (local indoor and outdoor spaces for transit and social-cultural interactions, public or private, with natural physical features (river, lake, terrain).

2. Materials and Methods

2.1. Earth Seasons: From Stable Mean to Asymptotic Patterns of Susceptible, Infectious, or Recovered (SIR) Modeling Equation

To better understand the terms used in this article, spreading patterns is considered as the type of transmission that COVID-19 may assume, be it airborne or physical contact. In contrast, dissemination patterns are understood as the cumulative daily new COVID-19 cases worldwide caused by the existent transmission forms. To set COVID-19 dissemination patterns under the Earth seasonality aspect of analysis, the endemic free-equilibrium of COVID-19 needs to be applied to Floquet Theory, currently employed in many other infectious diseases with a defined time period (T) of Earth seasonality (ε). To perform this task from a mathematical view of the problem, it is necessary to meet an oscillation to predict endemic R₀ under periodic and defined A(t) criteria, even for time-varying environments with no heterogeneity forces, thus assuming a linear force of infection with homogeneity as \( F(T) = B(t) \frac{\epsilon}{\tau} \). This would allow establishing a reasonable R₀ periodical stability for COVID-19 worldwide, as observed by Bacaër [12].

The stability point pre-assumed, if COVID-19 worldwide would be seasonal in winter as flu, could be defined as \( p(t + 1) = (A(t) + B(t))p(t) \) [12], with \( p \) representing the spectral matrix of periodicity \( A(t) \) and \( B(t) \) the environment of compartments S, I, and R of the SIR model (ecological variables such as biotic and abiotic of each country). Following this definition, the seasonality of COVID-19 at S, I, and R compartments are assumed to be dependent on deterministic outcomes for immunity, forms of transmission, healthcare interventions, and public policies under atmospheric triggering conditions (Earth seasons ε) as found, for example, in common flu. Considering this condition, the ODE (ordinary differential equations) could be easily observed in linear time series, as pointed in Sietto [13] as \( y(t) = a + bt + \sum_{i=1}^{m} c_i \cos \theta + \sum_{i=1}^{n} d_i \sin \theta + \epsilon(t) \), where the proposition of periodicity \( \theta \) as linear in time as \( B(t + T) = B(t) \) would be possible and consistent in its fluctuations in terms of daily new infections with seasonal sinusoidal patterns as \( \theta(t) = \theta_0 [1 + \epsilon \sin(2\pi t)] \) [14]. This could also be considered for stochastic expressions over time, considering seasonal fluctuations defined as hidden Markovian chains as \( P(Y(t) = y(t)|Y(t-1) = y(t-1), Y(t-2) = y(t-2), \ldots, Y(1) = y(1)) \) [13] and its many derivations, found in many studies [15–17]. This deterministic approach for the worldwide event would lead to the seasonal Fourier transform fluctuations of COVID-19 outbreaks, control, and over determined periodic cycles with no confounding scenarios. Fourier analysis would then be possible to perform considering time-periodic fluctuations as noted in Mari et al. [14]. Therefore, the use of Markovian chains to obtain the phase shifts of regularities would be a true approach to predict how SARS-COV-2 dissemination patterns are formed, regardless of spreading patterns. The main issue is when the stochastic process \( Y(t) \) assumes a lack of synchrony due to random worldwide delays and uncertainty [8,18,19] due to spreading patterns and characteristics of each country, region,
and place. This situation generates a stochastic form with unknown seasonality of infection, defined as $R'_0 = D \int_0^1 B(t) dt$ [18], and thus not assuming seasonality dissemination for $\varepsilon$ and the outbreak of local epidemics. At this point, it was observed that there are several discrepant (heterogeneous) time series of daily new infection cases in countries during 2019 and 2021 that were entering winter in the southern hemisphere and summer in the northern hemisphere. No great difference was verified at Earth dissemination seasonality influencing those localities [2,8,9,11].

The lack of dissemination pattern formation for COVID-19, as not found in common flu [20,21], creates an undefined $T$ over defined $A(t)$, as well as, a mean $\mu$ over periodicity $\theta$ criteria as a pre-assumption of analysis in Fourier’s perspective transform. This confirms an unexpected seasonality forcing behavior $\varepsilon'$ in which each sample (countries, regions, places) presents a different SARS-COV-2 dissemination pattern not only concerning the Earth seasonality but other components included in $\varepsilon'$.

2.2. Skewness Validation and SIR Model Limitation

What can be observed in many results [2] is an asymptotic unstable behavior of SARS-COV-2 dissemination patterns towards atmospheric conditions (temperature, humidity, ultraviolet (UV), and wind speed), policies and urban spaces that for this latter feature, differ greatly around the globe; and therefore not following only the Earth environmental seasonal forces as found in common flu [22–24]. The asymptotic feature of the phenomena relies on how virus transmission can be associated with a mixture of variables that sustain an indeterminate pattern of growing or reduction among countries. Worldwide, countries are facing daily new COVID-19 cases and the reason for countries to reduce its dissemination patterns are caused mainly due to HPALE on population [2–8] than a well-defined Earth seasonal period of COVID-19 transmission, as it is known that individual behavior and government policies are a major determinant for the pandemic peak reduction. This overall pandemic scenario could be observed in late March and starting in April 2020 when China and South Korea were the unique countries with the lowest rates of exponential growth of infection cases due to the type and strength of adopted HPALE [3,6], while Europe was in its fully active growing pattern. However, this does not mean that environmental variables such as atmosphere properties or Earth seasonality do not present causation of the event. It implies that HPALE influences the phenomenon at its beginning and end with a persistent pattern [2–8] rather than what was expected to be addressed only by the environmental factors as the main driving force of seasonality during winter periods. For this reason, constant COVID-19 dissemination is expected during all Earth seasons and HPALE can be one of the main seasonality driven force observed worldwide.

To add to this scenario, it is possible to identify one more important feature of pandemics, the urban spaces found in every city which present specific potential to influence local epidemics and mathematical simulations of SIR equations, namely the S and R compartments. This impact is due to the effects on each country/city/locality’s capability to deal with the outcomes of susceptibility, immunity, spreading patterns, and public health control measures, thus making COVID-19 predictive models assume data that do not correspond to reality. For each predictive model that fails to address urban spaces heterogeneity, HPALE interventions subjectivity, and environmental non-homology of data, the uncertainty degree grows. This leads to SARS-COV-2 emerging under unknown contagion patterns as observed in Billings et al. [19] and with a similar example of measles in Grenfell et al. [25].

2.3. Mathematical Framework of Three Seasonality Forcing Behavior of Coronavirus Disease 2019 (COVID-19) Worldwide and SIR Model Variants Needed

The unexpected seasonality $\varepsilon'$ under heterogeneity forcing behavior explain the exponential behavior of infection spreading patterns among countries an unpredictable sinusoidal expression such as $\beta(t) = \beta_0(1 + \varepsilon \varphi(t))$, as modelled by Buonuomo et al. [26] with a possibility of using Fourier transforms use, considering finite time lengths of analysis
(seasons) equally distributed over the period $T$ within samples (countries). This mathematical framework of analysis applies to the data series of daily new cases when these data present high-amplitude noise, often related to the lower spectral density and lower frequency that makes the analysis imprecise as a sinusoidal stable behavior in the basis form of Earth dissemination seasonality as $\int_{-\infty}^{\infty} f(t) \, dt$. In this sense, the sinusoidal behavior does not exist regarding how countries might present default oscillations within seasonal periods of Earth, as represented schematically in Figure 1.

![Figure 1. General framework of coronavirus disease 2019 (COVID-19) seasonality under the view of Fourier transform use limitations.](image)

Considering the aspects mentioned before, it is possible to observe that each sample can be understood as the lack of spreading and dissemination patterns towards the confident interval and standard deviation under default periods $T$ from 31 December 2019, to 3 March 2021, resulting in a stochastic maximum exponential form of daily new infections as $Y(t)$ changes over time, as already observed in the literature [2,8,27,28].

However, despite this scheme pointing to the weaker Earth seasonality forcing behavior of SARS-CoV-2 dissemination patterns, it can still influence the overall hidden transmission patterns due to HPALE interventions, environmentally driven seasonality, and urban spaces. This point can be addressed as a pattern formation $\varepsilon'$, of each sample, of confounding forced seasonality that dismantles S and R compartments of SIR predictive model over time [1,27–34], caused by environmental driven factors, urban spaces [35–37], and health HPALE intervention [2–8]. Then, it is possible to observe that each country might respond differently to the same initial conditions [8], influenced by the three components mentioned above, thus generating multiple patterns formation over time $T$ for SARS-CoV-2 forms of transmission and periodicity.

2.4. SIR Model Redefinition from the Original Equation to Skewness Patterns and Global Sensitivity

Concerning a theoretical desired worldwide SIR model normal distribution that most mathematical models imply for infection spreading and dissemination patterns with shape behavior $k = 1$ or $k > 1$ (Weinbull parameterization) of the exponential “regular” distributions of SARS-CoV-2 infection within time intervals $t$ and with defined periodicity $T$ (possible seasonality forms among countries) [38], the original defined form of $I$ compartment of SIR modeling equation is given as $\frac{dI}{dt} = \beta \frac{SI}{N} - gI$. However, the high asymptotic instability [27–34] of infected individuals ($I$) and the confounding scenario lead to redefining the equation’s basic fundaments to make the skewness analysis. Following
this sense, the I compartment of the SIR model was modeled to support confounding data as
\[
I = \left(\frac{\omega}{\lambda}\right)^k
\]  
(1)
where the infected \( I \) is influenced by the unpredictable scale of infection \( \lambda \) (\( N \)) for each sample with inconsistent behavior of variables for \( S \) term of the equation, thus influencing the transition rate (\( \beta \)) defined as \( \omega \) dissemination patterns (no global solution). Also it is not assumed for \( S \) in the original form of \( R \) compartment, that there is a normal distribution output for this virus spreading and dissemination patterns. This new dissemination pattern formation of the epidemic behavior was also described by Duarte et al. [39] when the contact rate does not encompass weather conditions and time-varying aspects of epidemics. Therefore, an unpredictable shape \( k \) of probabilistic outcomes (close to reality shapes) was used, mainly defining this shape caused \( \lambda \) and \( \omega \) asymptotic instabilities generated by \( S \) and \( R \) compartments over time [1,27–34], among the environmental- and urban space-driven factors [35–37] and HPALE interventions [2–8]. This equation represents the presence of confounding and heterogeneous environmental variables \( \omega \) with an unknown predictive scale of \( \exp \lambda \) or maximum likelihood estimator for \( \lambda \) due to non-linear inputs for \( S \) and \( R \) compartments over time as a global proposition (urban spaces, HPALE, and environmental conditions influence), thus generating nonlinear outputs \( k \) (asymptotic instability) [40,41]. If it is considered that most models are searching for a normality behavior among countries, hence, implying that the \( k \) distributions are non-complex and not segmented by its partitions, thus resulting in linearity for the virus infection \( I \) over \( Y \) and \( t \), then the overall equation as described by Dietz \( \beta(t) = \beta m(1 + A \cos(\omega t)) \) [40] would not be reachable for any given period of analysis considering the seasonality forcing behavior of SARS-CoV-2.

The outputs with heteroscedasticity and non-homologous form for \( k \) and \( \lambda \) can be modified to reach stable points of analysis, as modeled by Dietz \( \beta(t) = \beta m(1 + A \cos(\omega t)) \) for each of the three seasonality forces influencing SARS-CoV-2 spreading patterns. These three stable points of the asymptotic structure mentioned before can be observed in Figure 2.

![Figure 2](image_url)

**Figure 2.** Severe acute respiratory syndrome coronavirus 2 (SARS-CoV-2) spreading and dissemination patterns filtered and stated as expressing within the three phases of the epidemic: environmental spreading and dissemination patterns, health policies and adult learning education (HPALE), and the urban spaces dissemination patterns.

To remove heteroscedasticity and non-homologous form for \( k \) and \( \lambda \) from occurring in the three phases mentioned in Figure 2, as far as the \( k \) < 1 Weibull parameterization aspect [42] (Bell curve shape) of distribution is chosen as the most reliable region of analysis (attractive orientation) for any given \( T \) periods within any sample (countries daily new cases time series), it is necessary to modify the first Equation (1) to
\[
I = I = \left(\frac{Y(t)}{T}\right)^{k<1} - \left(\frac{\omega}{\lambda}\right)^k
\]  
(2)
hence with the new SIR model proposition as \( I = I' - (S + R) \), where \( I \) is asymptotically stable to \( I' \) and \( S \) and \( R \) considered in its original form \( \theta(t) = \theta_0[1 + e^{\sin(2\pi t)}] \) [14]. This is a mandatory redesign since many scientific breakthroughs point to health policies as the best approach to reduce COVID-19 [2–8]. Starting with this redesign of the equation, it is possible to find one of the first regions of analysis and stability that is health policy intervention, found in the slope (peak) of daily cases over time.

2.5. Birth and Death Persistence of COVID-19 Dissemination Patterns: From Positive to Negative Skew

Considering the new scope of analysis regarding time-series data mentioned before, it is now necessary to uncover the graphic regions in which confounding scenarios can be dismantled with a more robust relation of cause and effect according to Equation (2). It is important to address this birth and death persistence homology for this research, in which the desired mean function \( Y(t) \) of topological space \( X \to \mathbb{R} \) over \( \beta(t) = \beta m(1 + A \cos(\omega t)) \) indicated at (2) can be found as a persistence diagram existence [43] by mapping each adjacent pair to the point \((f(Y), f(t))\) local minimum and maximum observations, due to worldwide epidemic growth behaviour and subtle reduction due to HPALE measures. This step results in critical points of \( Y \) function over time \( t \), not in adjacent form globally but regionally triangularly space as \( d(D(Y_t), D(t)) \leq \| Y_t - t \|_{\infty} \) [44] with a given mean region, thus expressing random critical values (dissemination patterns) defined by \( I' = \left( \frac{Y(t)}{t} \right)^{k<1} \) in the real-life form of the event. However, since it is necessary to filter \( f(Y_n) - f(t_n) = y_n \) unstable critical points (oscillatory instability of seasonality for \( S \) and \( R \), HPALE, environmental driven variables, and urban spaces) to an attractive minimum behavior with normal distribution, these regions of analysis must be situated between \( \pi < y_n < \frac{\pi}{2} \) for every \( A(t) \to T \) asymptote period. Following this path, and roughly modelling it, the mean \( \mu(A(t)) \) is obtainable as the size of birth and death persistence diagram and triangulable diagonal (\( \Delta \)) like \( D(Y_t, t - \Delta) = \sum_{\pi < y_n < \frac{\pi}{2}} \mu^Y_{t} \) with multiplicity pairing regions \((t, Y_t)\) for each desired triangulation as \( 0 \leq t < Y_t \leq n + 1 \), resulting in the general equation for any assumed region as \( \mu^Y_t = \beta(t)\epsilon_{t_{i-1}}^\epsilon_{t_{i}} - \beta(t)\epsilon_{t_{i}}^\epsilon_{t_{i-1}} + \beta(t)\epsilon_{t_{i}}^\epsilon_{t_{i+1}} - \beta(t)\epsilon_{t_{i+1}}^\epsilon_{t_{i}} \) [44]. Note that each mean function \( \mu^Y_t \) will be given by regions defined as \( \beta(t) = \beta m(1 + A \cos(\omega t)) \), being \( \beta(t) \) the covariance function of seasonality forcing behavior of dissemination patterns formed by \( \mu(A(t)) \) under each \( \beta(t) \) form with \( \epsilon' \) partitions, hence without a global mean value for the event in terms of infection and time, or in other words, spreading and dissemination patterns. Further derivations and formulations regarding this persistence diagram will not be addressed for this research. However, it is recommended that future research keep this formulation defined for predictive and monitoring analysis of epidemic seasonality forcing behavior.

It is necessary to understand that this new design of seasonality regions can now be adapted adequately to Fourier transform analysis under the amplitude of waves with the equation \( e^{\pm i\omega t} = \cos(2\pi t) + i \sin(2\pi t) \) where angular momentum was drawn in the limits of \( \beta(t) = \beta m(1 + A \cos(\omega t)) \), giving \( \omega = \pi < y_n < \frac{\pi}{2} \) and generally defining it with sinusoidal reduced form as \( f(e') = \int_{-\infty}^{+\infty} Y(t)e^{-2\pi i\omega t} d\omega \) to reach a sinusoidal approach of time series data extraction and analysis over periods \( e' \) and given analysis regions.

Beyond the limitation of periods for predictive analysis and monitoring as a Gaussian process in the overall data of the given epidemics, the design in this article introduces one main point of analysis that is the lack of a global mean and covariance function \( \mu(Y(t)) \) over fluctuations as a global homomorphism and a decomposition form of wave signals similar to Fourier transforms. This occurs since spreading patterns of infection find heterogeneity within the type of HPALE interventions influenced by the confounding scenario created by the environment and urban spaces where persistent homology and homotopy cannot be found for \( t \cdot \kappa < 1 \) Weibull reliability to be situated globally for the overall times series data of epidemics in the oscillation-pairing regions of \( \sin(\pi t) = 1 \) and \( \cos(\pi t) = 0 \) for \( T \) desired coordinates of persistent fluctuations in \((f(Y_n), f(t_{k<1})) = y_n \) of stability can differ
over an extended time of analysis. HPALE range of influence is no longer stable (weak boundaries points of persistence), and therefore assuming \( t + 1 \) discrete form, defined as \( y_n = f(f(Y_n), f(t_{k+1})) \int_0^\pi \mu \sum(Y_0, \ldots, Y_n) dt \). However, by contrast, it can be found with continuous form as \( \delta = f(Y_n, t) \int_0^\pi \mu \sum(Y_0, \ldots, Y_n) d\mu \) [9], thus assuming the shape and limit to \( \kappa < 1 \) as small partitions \( \epsilon' \) to the desired analysis or without a derivative form for the overall analysis within the whole epidemics behavior observed. Considering the new partitions \( \epsilon' \), for the discretized view of \( Y_i, t \) as pointed out in the results of Roberts et al. [9], it is now possible to obtain a sample mean as a mode like \( \bar{Y} = \frac{1}{n} \sum Y_i, t \). Further results of this approach can be visualized at [9] Roberts et al. reference.

By rejecting the persistence diagram’s unstable critical points generated globally, a local minimum of the event as an average mean \( \epsilon' \) can be obtained by having \( Y(t) \) with the higher number of samples \( Y \) (daily infections) that finds a condition roughly described in the nonlinear oscillations within the exponential growth epidemic behavior of event as limited between maximum local growth defined by \( \frac{\pi}{2} \) by its half curvature oscillations \( \pi \) as a local minimum being non-periodic as \( 2\pi \) in a global homomorphism sense due to \( \kappa < 1 \). In this sense, the new sinusoidal approach offers a new mean function as an angular momentum of \( \pi \) for the analysis with a normal distribution, thus rejecting any critical value beyond \( \kappa < 1 \) for the desired coordinates \( \sin \frac{\pi}{2} \). Hence the wave-signal necessary to perform the Fourier transforms in each \( \epsilon' \) of data. This scheme can be observed for HPALE intervention on SARS-CoV-2 spreading and dissemination patterns [27] in Figure 3.

![Figure 3. HPALE stable region \( \epsilon' \) of analysis on SARS-CoV-2 dissemination patterns. Image data source: Worldometer—Italy on 8 July 2020.](image)

Therefore, \( Y(t), t \) assumes the desired oscillations samples and region conditions \( \epsilon' \) as \( \pi < y_n < \frac{\pi}{2} \) where birth and death persistent homolgy can be found for \( \kappa < 1 \). Considering samples’ time lengths, it is designed as \( t(\delta + 1) \leq f(Y(t)) \mu \sum(Y_0, \ldots, Y_n) dt \) starting from \( t_0, \ldots, t_n \leq \sin \frac{\pi}{2} \) results in the desired data distribution with a conditional shape of Weibull parameterization \( \kappa < 1 \) for the analysis with a normal distribution, thus rejecting any critical value beyond \( \cos \pi = \epsilon'_p \) and under \( \sin \pi = \epsilon'_p \), being \( \epsilon'_p \) the seasonality forcing behavior of HPALE intervention over SARS-CoV-2 among countries’ data sets. Concerning time lengths of samples, designed as \( t(y_n + 1) \leq f(Y_n) \mu \sum(Y_0, \ldots, Y_n) dt \) starting from \( t_0, \ldots, t_n \leq \sin \pi \) results in the desired data distribution, thus rejecting any critical value beyond \( \cos \pi = 0 \) and under \( \sin \pi = 1 \). The main reason to ignore S and R local solutions, or to not use SIR models globally, is also the same reason to adopt a region of analysis in the time series data for \( \epsilon' \) and HPALE. This also remains for the other two important inputs of the system derivatives (environmental factors that influence COVID-19 dissemination and urban spaces) of which for each country the aforementioned confounding scenario of analysis is shown in Figure 4.
Noting that the S and R compartments of the SIR model are needed for predictive analysis of infection dissemination patterns, these compartments might work properly under the third region of time series data: urban spaces $\varepsilon_u$ seasonality. To achieve results with a high uncertainty reduction, it is necessary to conceive S and R as in its most stable region of analysis, which should be influenced in a posterior scenario where $\varepsilon_p$ (HPALE) and $\varepsilon_e$ (environmental seasonality) already took effect. This is mandatory since, as far as policies are assumed in models or estimated with unreal quantitative parameters, uncertainty growth is promoted along with limitations to track real patterns within an urban space feature for S and R as a causation relation. For urban spaces seasonality forcing behavior, it is considered that inside and outside urban spaces promote limitations to HPALE due to the limiting action that it can face within these urban spaces (not all HPALE can reach some urban spaces features properly as it was designed to be). Environmental seasonality can also be present at this phase by influencing urban spaces limitations of taken HPALE actions. Therefore, $\varepsilon$, might find a growing point inside and outside urban spaces beyond $\varepsilon_p$ normalization (more explanation of this causation effect will be given in the Results section), which can be the cause of worldwide second waves or posterior waves.

Considering unexpected seasonal forcing $\varepsilon_p$ roughly defined as $\partial(t) = \theta_0 \left[1 \pm \varepsilon_0 \cos \pi < \varepsilon < \sin \frac{\pi}{2}\right]$ [9] in a complex network model, where no periodic oscillation (sinosoidal) are to be found in a discrete form with $f(\varepsilon_{p,u}) = \int_{\omega_0}^{2\pi} Y(t), t e^{-2\pi i \omega t} d\omega$, assume now a rupture of the $\sin(2\pi t)$, leaving the region the pre-assumed linearity $\theta(t) = \theta_0\left[1 \pm \varepsilon \sin(2\pi t)\right]$ for S and R in the overall metrics of time series data $T$ within one sample or among countries and understanding each iteration of the event as unconnected to the previous and future data if considering multiple time-series comparisons (among countries) or even in the same time series if considering long-term analysis. Since the $I'$ is an asymptote to $\varepsilon_p$, then $\varepsilon_u$ is limited by $\varepsilon_p$ on $I'$, but not necessarily fully stable in terms of $\varepsilon_p$ present total control over environmental seasonality due to urban space features.

It is possible to verify that most of these SIR models are constructed based on $\varepsilon_p$ seasonality behaviors [45–48]. Following this phase, urban spaces and HPALE interventions might present a strong influence on the outcomes due to the unpredictability of S and R patterns to design appropriate contact rates, which still represents a limitation for the SIR model methods [27–34]. Nonetheless, it is still the most desirable region of analysis for data extraction.

3. Results

The overall scenario of spreading and dissemination patterns skewness concerning the environment, HPALE and urban spaces can be visualized in Figure 5, where seasonality forcing behavior assumes the following topological metric space. Considering all

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**Figure 4.** Considering the observation COVID-19 confounding scenario, it is presented the asymptotic strong seasonality force of HPALE ($\varepsilon_p$) intervention and the narrow and unstable region (outbreak and control) of analysis for environmental and urban driving factors of seasonality ($\varepsilon_e, \varepsilon_u$).
the possible seasonality types, \( f(ε'_{c,p,u}) = \int_0^{+\infty} Y(t) \cdot e^{-2\pi \omega t} d\omega \), in continuous form of observation, with the need to discretize within causal roots of analysis due to heterogeneity and confounding scenario of analysis, HPALE seasonality can be understood as \( fε' = g \circ f(Y_t, t) = g(f(ε'p)) \), hence it can also be written as, \( fε' = h \circ (g \circ f(Y_t, t)) = h(g(f(ε'p))) \) as a control phase of local epidemics. However, this phase might present high instability (spreading patterns fluctuations) at a worldwide level due to heterogeneity and confounding behavior of \( fε'_{u} \) and \( fε'_{c} \). Since SIR models require stable points for S and R, there is \( fε'_{u} = h \circ g(Y_t, t) = h(g(ε'_{u})) \), resulting in a stable asymptotic convergence only if \( fε'_{p} = h \circ (g \circ f(Y_t, t)) = h(g(f(ε'p))) \). Since the outbreak might incur in unknown spreading and dissemination patterns for \( fε'_{p} \), \( fε'_{e} \) and \( fε'_{u} \), this region needs to be carefully considered. Therefore, environmental seasonality can be found as \( fε' = (h \circ g(Y_t, t)) \circ f = f(h(g(ε'_{e}))) \) or it is also possible to assume \( fε' = (ε \circ g(Y_t, t)) \), being \( ε \) the undefined patterns of environmentally driven new infections for Earth seasonality or atmospheric factors, which was not fully resolvable in this research.

\[
(h \circ g) \circ f = \text{outbreak}
\]

\[
h \circ (g \circ f) = \text{control phase}
\]

Figure 5. Schematically representation of the COVID-19 skewness properties: during epidemics evolution, HPALE influences the environment and urban spaces seasonality until a limit defined by its type and strategy of application; compartmental models during peak phase are influenced by HPALE, environment and urban spaces and present high uncertainty; at control phase, policies/HPALE finds its limitation by the environment and the type of urban spaces and finally, at outbreak, environmental factors present outcomes caused by the existing HPALE and urban spaces.

4. Discussion

Concerning urban spaces’ spreading patterns, due to the vast diversity of public health infrastructure buildings design, outdoor and indoor building designs within natural physical features such as rivers, lakes, snow, culture, and urbanization developments, they exert influence on the region of environmental driven pattern and not only policies. Therefore, it is reasonable to understand that any assumption on S and R during the epidemic phase in its initial curvature is much more closed to uncertainty measures than ever due to several possible confluences. Countries may then diverge greatly in the urban space and environmental scenarios, and thus S and R compartments face calculation limitations during peak curvature, being uncertain how to predict virus spreading and dissemination patterns since policies/HPALE are not even fully developed or had adequate time to take effect while most of the models use policies as the basis of modeling the dissemination patterns. For this reason, the most reliable region of analysis for these compartments and where most of the models are currently situated/functioning remains at the control phase of epidemics. However, fluctuations may still occur worldwide due to
the type of HPALE and urban space features. Therefore, urban spaces and environmental seasonality drivers are the main cause of aperiodic and unstable behavior for SARS-COV-2 spreading patterns worldwide. It is likely that environmental driven seasonality results found in many studies are, in truth, HPALE and urban spaces results, representing a need for further detailed research [48].

This was addressed in the research [49], where despite the vast review made, and the observation of confounding scenarios for each sample of analysis and type of climate conditions that influence COVID-19 spreading patterns, authors [49] have understood that there are homogeneity and heterogeneity in the statistical results and conclusions about the environmental influence on the virus dissemination patterns. This was addressed correctly in a systematic review [49] and further developed in this present study through a careful observation that environmental influence can be better understood in outbreaks and urban spaces by using graph analysis. Also, despite the analysis made in [49] considering only policies and climate conditions, further scenario need to be evaluated that is urban spaces, where human lifestyles are directly connected with a risk behaviour over contamination of infectious diseases, such as COVID-19, hence human behaviours also have great impact in the preventive measures efficacy.

Also, concerning evolutionary and game of life algorithms [50,51], predefined parameters and initial inputs are crucial for the machine learning analysis. However, beyond biological features as described in the last paragraph, unpredictable scale of infected individuals are found worldwide without vaccination or social isolation. The article aimed to analyze the problem without these predefined parameters being the basis and sensitivity of analysis. This can be mandatory since many countries are facing problems with vaccination speed and availability as well as social isolation as well as a severe lack of citizen compliance in many countries. Similarly, in Bateman SIZ analysis, this approach can be observed [52] regarding the uncertainty of models without using predefined parameters for sensitivity and robustness. These uncertain parameters lead the calculations to include new panoramic idea of how to combat COVID-19 without proper pre assumptions, thus giving for the real world skewness observed in predictive methods, a degree of uncertainty worldwide. This can be useful due to the lack of correlation between the sensitivity of models and real life complexity.

Concerning uncertainty and sensitivity, the article presents some references that address this point [8,30,33,45]. This research’s main objective was to analyse the SIR model equation without pre-defined data input in terms of formulating a specific SIR model to perform predictive analysis with numerical results. For this reason, theoretical observations were made, considering references findings and the global sensitivity model used (policies and ALE, environment and urban spaces). Despite not considering numerical solutions of the problem, due to complexity issues for data collection in real life and chaotic behaviour of some events, the theoretical model proposed can be helpful to understand how pandemics should be investigated for future SIR model equations and also for the basic interpretation of epidemiological behaviour of SARS-COV-2. This is mandatory nowadays since many countries present unfitted vaccination prediction, unfitted social isolation prediction and unfitted SARS-COV-2 variants appearance. The validation of the data subject can be found in Section 2.2. Skewness validation and SIR model limitation. Since the model proposed in this article is not developed to numerical data or results, the theoretical basis of analysis was retrieved from references that already performed these numerical solutions of the problem. Therefore, compiling these findings, it was possible to observe how skewness properties of the issue express how the virus behaves worldwide without predefined spreading and dissemination patterns. This concept of an absence of predefined spreading and dissemination patterns was supported in the results section, aiming to describe how uncertainty and predictive constraints can be found based on the SIR model equation and its variants developed worldwide.

In the research results section, it is possible to observe that the most reliable region to investigate environmental seasonality remains at the outbreak and control phases. In
contrast, best urban space seasonality observations remain at the control phase. This feature can be very useful for HPALE approaches since the actual fluctuations/instability in the region mentioned above are mainly caused by these two posterior forcing behaviors. Therefore, new strategies and measurements need to be adopted to keep the economy and prevention with similar power, which was already initially investigated by Sajadi et al. in June 2020 [46].

Note that there is a great difference between environment-driven seasonality caused by urban spaces influenced by HPALE limitations or otherwise caused by Earth and other natural (atmospheric) seasonality forcing behavior at outbreaks. This characteristic should be carefully considered when studying Earth seasonality among countries. The compartmental models are mostly in the control phase region and lose efficacy at outbreaks where no specific parameters are given, and environmental seasonality is not yet discovered in its true patterns. Another point regarding the control phase is that in which instabilities can occur, as far as urban spaces create a scenario where HPALE faces limitations, environmental seasonality finds a suitable place to grow its patterns [47]. Due to uncertainty growth over time and the lack of mean for defined intervals of $t$ over $T$ normal distribution shape for the whole data, Earth season $\epsilon$ gradually loses its effect with the possibility of random delays observed for each country of analysis (sample) being attributed by different patterns in which an outbreak occurs since existing HPALE are found within worldwide cultures, science, and education.

5. Conclusions

This research modeled SARS-COV-2 spreading and dissemination patterns sensitivity by defining and redesigning time series data extraction to SIR model equations. The approach opened a new scenario where seasonality forcing behavior was introduced to understand SARS-COV-2 skewness expressions due to heterogeneity and confounding epidemics scenarios where actual SIR models might find a high degree of uncertainty caused by oscillatory conditions found in the input of variables of the event.

The main research results are the elucidation of three birth and death forced seasonality phases that can explain how COVID-19 spreading and dissemination patterns skewness occurs worldwide. It can be understood in the following order: (1) the environmental variables (Earth seasons and atmospheric conditions); (2) health policies and adult learning education (HPALE) interventions; (3) urban spaces (local indoor and outdoor spaces for transit and social-cultural interactions, public or private, with natural physical features (river, lake, terrain).

These three forced seasonality phases were pointed to as the most effective explanation concerning uncertainty found in the predictive SIR model equations that might diverge in outcomes expected to express the disease’s behaviour. Therefore, many distinct models were generated to cover COVID-19 confounded scenarios.

Regarding the forced seasonality model the following pattern was observed: HPALE can be the strongest stable point of seasonality during the epidemic peak phase and compartmental models are influenced mainly by HPALE, while environmental and urban spaces present a low or hidden influence on it. However, HPALE can still be limited at the control phase, depending on urban spaces and existing environmental conditions demanding SIR models to adapt to these new features. Finally, at outbreak and control phases, environmental factors present outcomes caused by the existing HPALE and urban spaces of a given sample, thus producing high uncertainty to predictive SIR model equations.

6. Limitations

ALE was considered in the view of effective practice mainly based on adequate policies adopted by countries. Nonetheless, it should be carefully addressed in the view of infodemics practices, in which ALE can assume one more seasonal force in epidemics, disrupting the peak and control phase and promoting new spreading and dissemination patterns during $\epsilon_p$ seasonality. It can also enforce posterior waves and confirm spreading
pattern fluctuations at outbreaks and urban spaces’ stability and, therefore, demanding new modifications in SIR models.

**Author Contributions:** Conceptualization, C.R.T.; Methodology, C.R.T. and H.L.; Formal analysis, C.R.T.; Investigation, C.R.T.; Resources, H.L. and C.R.T.; Writing—original draft preparation, C.R.T.; Writing—review and editing, D.F., H.L. and C.R.T.; Supervision, H.L.; project administration, H.L.

All authors have read and agreed to the published version of the manuscript.

**Funding:** Sponsored by social responsibility programme by Sharen to support COVID-19 open source publication.

**Institutional Review Board Statement:** Not applicable.

**Informed Consent Statement:** Not applicable.

**Data Availability Statement:** Some of the data used are available at Our World in Data and Outbreak website retrieved from: https://outbreak.info/data and https://ourworldindata.org, respectively.

**Acknowledgments:** The author feels very grateful for the researchers that made this article possible through conversations and revisions: Ralf Reintjes (Department of Health Sciences—Hochschule für Angewandte Wissenschaften Hamburg—Hamburg), Ana-Maria CEAUP Universidade do Porto; UNDP) and Manuel Hernández Rosales (Universidad Nacional Autónoma de México).

**Conflicts of Interest:** The authors declare no conflict of interest.

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