CFD INVESTIGATIONS OF THERMAL AND DYNAMIC BEHAVIORS IN A TUBULAR HEAT EXCHANGER WITH BUTTERFLY BAFFLES

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ABSTRACT

In the present paper, the effects of a new baffle design on the efficiency of a tubular heat exchanger are numerically investigated. It concerns butterfly baffles inserted in a cylindrical tube heat exchanger. We focus on the influence of the shape of baffles, the space between baffles (pitch ratio, PR) and the baffle size (i.e. the blockage ratio, BR) on the heat transfer and flow characteristics. Three geometrical configurations with different PRs are realized (PR = 1, 2 and 4) and five others with different blockage ratios (BR = 0.1, 0.2, 0.3, 0.4 and 0.5). The investigations are achieved for Reynolds numbers ranging from 3000 to 8000. All analyses are realized with the help of the CFD Fluent software. The numerical results are compared with available experimental data and a satisfactory agreement is found. The obtained results showed that the butterfly baffle with PR = 4 and BR = 0.1 is the best design that ensures the best flow mixing and increases the thermal enhancement factor by about 1.7 time with a moderate pressure drop.

Keywords: Tubular heat exchanger; Butterfly baffles; Heat transfer; Fluid flow; pressure drop

1. INTRODUCTION

A heat exchanger with a reduced cost, a compact size and with high thermal performance is very required in many engineering systems such as nuclear central, vehicle, refrigeration, solar air heater and several chemical engineering processes. Hence, the heat exchanger design plays a great challenge to overcome the problems of the lower performance. A successful technique for enhancing the heat transfer performance is using baffles/ribs or vortex generators (VGs). The presence of baffles helps to stop the thermal and hydrodynamic boundary layers and intensifies the turbulent flows. However, the use of baffles augments not only the heat transfer coefficient but also it increases significantly the pressure drop.

Until present, studies continue not only to optimize the design of baffles. Some researchers interested to the baffling in channels for different industrial applications such as for the solar energy applications Promvonge et al. (2011) and Kumar, Kim (2015) , gas turbine cooling Giovanni (2004), sedimentation tanks Al-Sammarraee et al. (2009) and Agharzadeh et al. (2011) . Among others. In experimental studies, Han et al. (1991),(1992) examined the heat transfer phenomenon in a square channel with different attack angles of ribs on two walls for the pitch ratio (P/e = 10) and the blockage ratio (e/D = 0.0625). They reported that the angled ribs with ‘V’ shape have a great effect on the heat exchanger performance. Torri et al. (2002) used delta winglet-type baffles in a fin-tube heat exchanger with rounded tubes and found a great improvement in heat transfer and a reduction in friction factor. Wang et al. (2002) studied experimentally the effect of baffles on the flow structure and heat transfer in a fin-and-tube heat exchanger. They obtained a decrement of pressure loss tend to 25–55% compared with the flat fin arrangement.

The orientation angle of baffle has an important effect of the heat transfer execution and the inclined baffle may give an enhancement by more than 30%, as reported by Promvonge et al. (2014). Depending on the blockage ratio (from 0.05 to 0.3), Promvonge et al. (2010) revealed that the baffles with 45° attack angle increases the heat transfer coefficient from 150% to 850%. In the same field, Kwankaomeng et al. (2010) tested numerically the effect of 30° inclined baffles with different values of BR on the fluid flow and heat transfer. They showed that the 30° angled baffles produce the vortex flows and augment significantly the heat transfer coefficient in the channel. However, the heat transfer increase as associated with important pressure drop ranging from 1 to 17 times above the channel without baffles. The horse shoes baffles used by Promvonge et al. (2015) in tubular heat exchangers offered a considerable improvement of heat transfer coefficient tend to 92-208%, but with an increase in the friction factor about 1.76 to 6.37 times compared with the smooth tube, i.e. a thermal performance factor varied from 1.34 to 1.92.

The perforated baffle is another significant topic in heat transfer execution like underlined it Islam et al. (2010) and Bhuiyan et al. (2016).In the goal to reduce the lower heat transfer areas (LHTAs) behind the baffle, Sahel et al. (2016) proposed a perforated baffle having a row of four holes placed at three different positions (the so called pores axis ratio (PAR)). From all cases studied by these authors (PAR = 0.190, 0.425 and 0.660) the first case is found to be as the best one. This article presents a new baffle design for tubular heat exchangers. It concerns baffles with a butterfly shape. We explore the
efficiency of the new suggested design by changing its size (i.e. the blockage ratio) and the space between baffles (i.e. the pitch ratio).

2. FLOW AND BAFFLE GEOMETRY

The geometry of the problem studied concerns a circular tube with butterfly baffles (Figs. 1 and 2). Air is used as a working fluid. The tube length (L) is equal to 1000 mm and its diameter (D) is set to 50 mm. Effects of the baffle size (e) are investigated by realizing five geometrical configurations (e = 5, 10, 15, 20 and 25 mm) which correspond to the following values of the ratio e/D (the so called blockage ratio, BR = e/D): 0.1, 0.2, 0.3, 0.4 and 0.5, respectively. Effects of the space between baffles (i.e. the pitch P) are also examined by realizing the following series of grids: 844191, 978575, 1040998, 1157849 and 1290049 elements.

Effects of the space between baffles at the inlet and the outlet sections of the tube to ensure the fully developed flow at the inlet and to avoid the appearance of reversed flows at the outlet.

2.1 Boundary Conditions

The velocity and temperature profiles are identified at the inlet section. A uniform air velocity \( U = U_a \) and a constant temperature \( T_a = 300^\circ K \) (corresponding to the Prandtl number \( Pr = 0.7 \)) were introduced at the inlet boundary, while an atmospheric pressure outlet condition was applied at the exit. The air physical properties are constants. No-slip wall condition is applied for the tube walls and the baffles. The temperature of all the tube walls is kept constant at 350° K while the baffles are assumed at adiabatic walls.

2.2 Mathematical Formulation

The duct flow is governed by the Reynolds averaged Navier–Stokes (RANS) equations and the energy equation. For incompressible turbulent flows these equations can be written as:

- Continuity equation:
  \[ \frac{\partial}{\partial x_j} (\rho u_j) = 0 \]  
  (1)

- Momentum equation:
  \[ \frac{\partial}{\partial x_j} (\rho u_i u_j) = \frac{\partial}{\partial x_i} \left( \mu \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \right) - \frac{\partial p}{\partial x_i} \]  
  (2)

- Energy equation:
  \[ \frac{\partial}{\partial x_i} (\rho u_i T) = \frac{\partial}{\partial x_i} \left( \Gamma + \mu \frac{\partial T}{\partial x_i} \right) \]  
  (3)

where \( \Gamma \) is the thermal diffusivity, it is given by:

\[ \Gamma = \frac{\mu}{\rho \eta} \]  
(4)

\[ \rho u_i u_j \] is the Reynolds stresses defined by the Boussinesq hypothesis (FLUENT, 2001):

\[ \frac{\partial}{\partial x_j} (\rho u_i u_j) = \frac{\partial}{\partial x_j} \left( \mu \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \right) - \frac{\partial p}{\partial x_i} \]  
(5)

Where \( \delta_{ij} \) is the Kronecker delta.

The k-ε standard model of turbulence which is based on the turbulent kinetic energy \( k \) (Eq. 6) and the energy dissipation \( \varepsilon \) (Eq. 7) is used in this study.

\[ \frac{\partial}{\partial x_j} (\rho k u_j) = \frac{\partial}{\partial x_j} \left[ \mu + \frac{\mu_\text{t}}{\sigma_\text{t}} \right] \frac{\partial k}{\partial x_j} + G_k + \rho \varepsilon \]  
(6)

\[ \frac{\partial}{\partial x_j} (\rho \varepsilon u_j) = \frac{\partial}{\partial x_j} \left[ \mu + \frac{\mu_\text{t}}{\sigma_\text{t}} \right] \frac{\partial \varepsilon}{\partial x_j} + C_{k\varepsilon} \frac{\varepsilon}{k} - C_{\varepsilon} \frac{k \varepsilon}{k^3} \]  
(7)

In these equations, \( G_k \) represents the turbulent kinetic energy generated by the mean velocity gradients.

The empirical constants for the are assigned the following values (FLUENT, 2001):

\[ C_k = 0.99; C_{k\varepsilon} = 1.44; C_{\varepsilon} = 1.92; \sigma_k = 1.0; \sigma_\varepsilon = 1.3 \]

The standard k-ε turbulence model is reliable and robust, with a higher convergence rate compared to other models, and it gives accurate results in the prediction of turbulent flow and heat transfer in the baffled channels (Promvonge et al. 2010, 2014, 2015 and Sahel et al. 2016).

The heat transfer is calculated from the Nusselt number \( (Nu) \) which can be obtained by:

\[ Nu = \frac{h D}{k_f} \]  
(8)

The Reynolds number (Re) based on tube diameter is given by:

\[ Re = \frac{U D}{\mu} \]  
(9)

The friction factor \( (f) \) calculated along the test tube length (L) is written as:

\[ f = \frac{2}{(L / D_h) \rho U_m^2} \right) \frac{\Delta P}{\rho U_m^2} \]  
(10)

The thermal enhancement factor \( \eta \) is defined by:

\[ \eta = (Nu / Nu_0) / (f / f_0)^{\gamma_3} \]  
(11)

Where \( Nu_0 \) and \( f_0 \) are the Nusselt number and friction factor for a smooth tube, respectively.

2.3 Numerical Method

The geometry of the system examined was created and meshed by using the Gambit software. A tetrahedral mesh element is selected for meshing the computational domain (Fig. 3). In this field, we can choose any type of mesh. Where the most important is the mesh sensitivity test which gives a high accuracy of results. In addition, the tetrahedral mesh is simple to generate in complex geometries. For the tube without baffles, mesh tests were realized with following series of grids: 487460, 594924, 766411, 882797 and 978575 mesh elements.

The accuracy of results is obtained from 766411 elements, where the variations of the Nusselt number do not go above 2% with further increases in the grid density. Hence, the final grid number which is adopted for the following investigations is 766411 elements. The same strategy was used for the other geometrical arrangements, where the adopted grids element was varied from 844191 to 1040998 elements.
FLUENT (2001), which is based on the finite volume method, is the commercial software used to simulate the fluid flow and heat transfer in the computational domain. The flow regime is turbulent and the tube flow model is governed by the Reynolds averaged Navier–Stokes equation with the standard k-ε turbulence model and the energy equation.

Investigations are considered steady and the flow regime is turbulent. The second order scheme is employed to discretize the convective terms in governing equations. For the pressure–velocity coupling, the SIMPLE algorithm (Semi-Implicit Pressure Linked Equation) is used. Default under-relaxation factors of the solver are used to control the update of computed variables for each iteration. These factors are: 0.3, 1, 0.7 and 1 for pressure, density, momentum and energy, respectively. The criterion of convergence is that the standardized residuals are below $10^{-6}$ for the flow equations and $10^{-9}$ for the energy equation.

Simulations were achieved in a computer with Intel core i7 including 6.0 GB of RAM and processor speed of 2.20 GHz. Convergence was obtained after 8000-14000 iterations with computational times of 4-6 hours.

3. RESULTS AND DISCUSSION

3.1 Validation of Predicted Results

The predicted results on the heat transfer and friction characteristics in a smooth tube are validated by checking the values of Nusselt number (Nu) and friction factor (f). With the same geometrical and operating conditions, our results were compared with those obtained by using the Dittus-Boelter’s (1930) and Gnielinski’s (1976) correlations for Nusselt number, Moody diagram (1944) and Gnielinski’s correlation for the friction factor.

The Dittus-Boelter’s correlation is:

$$Nu = 0.023 Re^{0.8} Pr^{0.4} \quad \text{For } Re \geq 10000.$$  \hspace{1cm} (12)

The Gnielinski’s correlation is:

$$Nu = \frac{(f/8) Re Pr}{1 + 12.7(f/8)^{1/2} (Pr^{2/3} - 1)} \quad \text{For } 2300 \leq Re \leq 5.10^6$$ \hspace{1cm} (13)

The friction factor correlation from the Moody diagram is:

$$f = 0.316 Re^{0.25} \quad \text{For } Re \leq 2.10^4$$ \hspace{1cm} (14)

The friction factor given by the Gnielinski’s Correlation is:

$$f = (0.76 \ln Re - 1.64)^2 \quad \text{For } 2300 \leq Re \leq 5.10^6$$ \hspace{1cm} (15)

Figs. 4a and 4b present the variation of Nusselt number and the friction factor vs. Reynolds number, respectively. The comparison of our numerical results with the other data shows a satisfactory agreement. As shown in the figure, the correlations of Gnielinski (1976) is merit to use in the validation of both Nusselt number in the smooth tube. Where, the deviation between the numerical results and those predicted by Gnielinski (1976) do not less 3% for the Nusselt number. For the friction factor prediction, both correlations of Gnielinski (1976) and Moody diagram (1944) give the same deviations of about 10%.
3.2 Flow Structure

The flow modifications due to the presence of baffle inside the tubes give more augmentation in the heat transfer coefficient of the heat exchanger. For \( BR = 0.4 \) and \( Re = 4000 \), Fig. 5 (a-d) shows the temperature distribution in a smooth tube and for different pitch ratios (PR = 1, 2 and 4). This figure clearly reveals the important change in the temperature along the tube walls, especially in the region behind the baffle, where recirculation zones are located. On the other hand, a weak temperature gradient is created in the other regions by swirling flows.

![Temperature contours](image)

Fig. 5 Temperature contours [°K] for (a) smooth tube, (b) PR=1, (c) PR = 2 and (d) PR = 4, at Re = 4000, BR = 0.4

Fig. 6 presents the distribution of the axial velocity for different values of the pitch ratio (PR = 1, 2 and 4), at BR = 0.4 and \( Re = 4000 \). As reported in literature, the flow structures influence directly on the thermal performance of heat exchangers. Moreover, the presence of baffles in the tubes of heat exchangers is also an important technique to enhance the heat transfer coefficients where these baffles help to stop the thermal and hydrodynamic boundary layers and intensifies the turbulence and the fluctuation velocity near the tube wall.

![Axial velocity distribution](image)

Fig. 6 Axial velocity distribution (in [m/s]), for (a) PR = 1 (b) PR = 2, (c) PR = 4, at Re = 4000.

3.3 Nusselt Numbers

The variation of Nusselt numbers versus Reynolds numbers for different baffles arrangement is presented in Fig. 7. In order to optimize the heat transfer execution, two baffle configurations are tested: the pitch ratio (PR = 1, 2 and 4) and the blockage ratio (BR = 0.1, 0.2, 0.3, 0.4 and 0.5).

Since the baffle creates swirling flows and intensifies the turbulence, the heat transfer coefficient for the baffled tube is generally higher than that for the smooth tube. In Fig. 4, the Nusselt number slightly increases with the increase of the pitch ratio (PR). Also, it clearly augments with the rise of the blockage ratio (BR) and Reynolds number (Re). With the optimal value of pitch ratio (PR = 1) and at \( Re = 8000 \), the heat transfer enhancements with the following values of the blockage ratio (BR = 0.1, 0.2, 0.3, 0.4 and 0.5) are about 27 %, 29%, 36 %, 40% and 32% above the smooth tube, respectively.

The higher heat transfer coefficient is obtained with the case (BR = 0.4, PR = 1 and \( Re = 8000 \)), where the Nusselt number value for this case is higher by about 40 %, compared with the smooth tube. Hence, the heat transfer coefficient in the tube with baffles under a butterfly shape is better than that for the smooth tube. This baffle shape offers a strong mixing leading to stop the formation of the thermal boundary layer.
3.4 Friction Factor

Habitually and because of the change in the flow direction and the velocity fluctuations near the wall, the augmentation of the heat transfer coefficient results in an increase of the friction factor. Effects of PR and BR on the friction factor are shown in Fig. 8(a-c). As observed, the friction factor decreases with the decrease of the blockage ratio (BR) and the increase of Reynolds number (Re) and the pitch ratio (PR). This is due to the dynamic pressure dissipation caused by the higher surface area and the act of the reverse/swirl flow. At Re = 3000 and for the optimal value of pitch ratio (PR = 1), the heat transfer enhancements with the following values of the blockage ratio (BR = 0.1, 0.2, 0.3, 0.4 and 0.5) are about 33%, 66%, 80%, 87% and 85% above the smooth tube, respectively.

However, at Re = 3000, the baffle case with BR = 0.4 and PR = 1 gives the greatest value of friction factor. For this case, \( f \) is greater by about 87% compared with the smooth tube. This is due to the blockage of flow and its contact with the large surface of baffle (BR = 0.4).
3.5 Evaluation of Thermal Performance

Fig. 9 shows the variation of the thermal enhancement factor (η) vs. Reynolds number for different baffle arrangements. The enhancement factor tends to increase with the rise of Reynolds number for various BR and PR values. Except the case with BR = 0.5, the thermal enhancement factor is higher than the unit for the others cases, indicating that the use of butterfly baffles is advantageous and efficient than the smooth tube. As remarked, the baffle with BR = 0.1 and PR = 4 presents the maximum enhancement factors (η) are about 1.7 to 1.5 with the rise of Re.

![Fig. 9 Variations of the thermal performance factor (η) with Re for various BR and PR](image)

4. CONCLUSIONS

The present paper summarized results of numerical investigations of the fluid flow and heat transfer characteristics in a tubular heat exchanger fitted with series of butterfly baffles as a new design under different blockage and pitch ratios. The numerical analyses were performed for a turbulent flow where the Reynolds number was ranging from 3000 to 8000. The obtained results have shown that the butterfly baffles ensure a good mixing of flows and intensifies the circulation of fluid particles inside the tube. The baffle with BR = 0.1 and PR = 4 give the highest enhancement factors (η) which are about 1.7 to 1.5 with the rise of Re. Therefore, this case merits to be used in designing the tubular heat exchangers.

ACKNOWLEDGEMENTS

The authors thank Dr. Yuwen hang for all discussions and technical assistance.

NOMENCLATURE

| Symbol | Definition |
|--------|------------|
| A      | Convection heat transfer area, m² |
| BR     | Blockage Ratio BR = el/D |
| Dh     | Hydraulic diameter m |
| F      | Friction factor |
| Gk     | Turbulent kinetic energy production |
| h      | Heat transfer coefficient, W m² K⁻¹ |
| k      | Turbulent kinetic energy, Joule |
| k₁     | Thermal conductivity, W m⁻¹ K⁻¹ |
| L      | Channel length, m |
| Nu     | Nusselt Number |
| P      | Space between two successive baffles M |
| Pr     | Prandtl number |
| PR     | Pitch ratio PR=P/D |
| Re     | Reynolds number Re = ρUDh/ μ |
| T      | Temperature K⁰ |
| u      | Mean velocity at the channel m s⁻¹ |
| u₁     | Axial velocity m s⁻¹ |
| u₁     | Vertical velocity m s⁻¹ |

Greek Symbols

| Symbol | Definition |
|--------|------------|
| η      | Thermal enhancement factor |
| μ      | Dynamic viscosity (kg s⁻¹ m⁻¹) |
| ρ      | Density (kg m⁻³) |
| ε      | Turbulent energy dissipation (m² s⁻³) |

Subscripts

| Symbol | Description |
|--------|-------------|
| in     | inlet       |
| out    | outlet      |
| w      | wall        |

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