Exploiting Direct Link in Two-Way Half-Duplex Sensor Network over Block Rayleigh Fading Channel: Upper Bound Ergodic Capacity and Exact SER Analysis

Phu Tran Tin 1, Tan N. Nguyen 2,*; Minh Tran 3; Tran Thanh Trang 4 and Lukas Sevcik 1

1 IT4Innovations, VSB-Technical University of Ostrava, 70833 Ostrava, Czech Republic; phutrantin@iuu.edu.vn (P.T.T); lukas.sevcik@vsb.cz (L.S.)
2 Wireless Communications Research Group, Faculty of Electrical and Electronics Engineering, Ton Duc Thang University, Ho Chi Minh City 70000, Vietnam
3 Optoelectronics Research Group, Faculty of Electrical and Electronics Engineering, Ton Duc Thang University, Ho Chi Minh City 70000, Vietnam; tranhoangquangminh@tdtu.edu.vn
4 Faculty of Electrical and Electronics Engineering, Ho Chi Minh City University of Food Industry, 140 Le Trong Tan, Ho Chi Minh City 70000, Vietnam; trangtranthanh1979@gmail.com

* Correspondence: nguyennhattan@tdtu.edu.vn; Tel.: +84-283-775-5028

Received: 18 December 2019; Accepted: 12 February 2020; Published: 20 February 2020

Abstract: Relay communication, in which the relay forwards the signal received by a source to a destination, has a massive consideration in research, due to its ability to expand the coverage, increase the capacity, and reduce the power consumption. In this paper, we proposed and investigated energy harvesting (EH) based two-way half-duplex (TWHD) relaying sensors network using selection combining (SC) over block Rayleigh fading channel. In this model, we proposed the direct link between two sources for improving the system performance. For the system performance analysis, we investigated and derived the closed-form of the exact and upper bound Ergodic capacity (EC) and the exact form of the symbol error ratio (SER). By using the Monte Carlo simulation, the correctness of the research results is verified in the influence of the main system parameters. From the discussions, we can see that the analytical and simulation agree well with each other.

Keywords: two-way; ergodic capacity (EC); energy harvesting (EH); SER; sensors network

1. Introduction

Radio frequency (RF) energy harvesting (EH) in wireless communications has recently attracted considerable attention which becomes particularly more attractive in applications where battery-limited devices are not easily accessible, and replacing or recharging their batteries is inconvenient, costly and/or unsafe such as devices embedded inside human bodies and wireless sensors operating under dangerous conditions. This solution is based on the fact that RF signals can concurrently carry information and energy, hence allowing energy-constrained nodes to harvest energy and process information simultaneously. This is referred to as simultaneous wireless information and power transfer (SWIPT). Motivated by this, nodes in future wireless networks are envisioned to be energy self-sufficient and more sustainable by harvesting RF signals from the surrounding environment [1–11]. The first basic idea about SWIPT was proposed in [12], in which wireless information and power transfer across a noisy coupled-inductor circuit. After that, other authors have studied the various communication network types based on the SWIPT for different system networks, such as the deployment of PBs for powering a cellular network via MPT investigated in [13], or the communication system network with
the single antenna receiver station for energy and information via power splitting protocol studied in [14,15]. In [16], the energy harvesting and information transmission in the wireless multi-antenna communication systems are investigated via a simplified three-node setup. The new wireless RF powered network with the H-AP harvested energy in the downlink and transferred the information in the uplink by TDMA is proposed and demonstrated in [17].

Furthermore, the cooperative relaying network has been deeply studied in the last ten years for improving the system performance of the communication network. The source and destination nodes can be communicated by helping the intermediate relay when the direct link between them is weak or with the long distance. The authors in [18] considered and investigated the outage probability of the three-node cooperative relaying network with a fundamental switching between energy harvesting and data relaying. The relay selection problem in the AF relay network with QoS and harvested energy constraints is proposed in [19]. In this paper, the authors investigated the dependence of the system ergodic capacity and the outage probability on the amount of energy transferred to the RF energy harvesters. In [20], the authors investigated joint wireless information and energy transfer in a two-user MIMO interference channel, in which each receiver either decodes the incoming information data or harvests the RF energy. Further, joint wireless information and energy transfer methods in a general K-user MIMO interference channel was studied in [21]. A wireless cooperative network with multiple source-destination pairs communicate with each other via an energy harvesting relay is presented in [22], and authors investigated the relay’s strategies to distribute the harvested energy among the multiple users and their impact on the system performance. In [23], the authors focused on the two-way amplify-and-forward relaying channels with an energy harvesting relay node. Here, the relay node harvests energy from signals from two sources and uses this energy for information transferring between them with amplify-and-forward mode. For multiple-input multiple-output relay channels [24], proposed a low complexity dynamic antenna switching between information decoding and energy harvesting based on the principles of the generalized selection combiner. The authors in [25] proposed and studied a cooperative multi-hop secured transmission protocol to underlay cognitive radio networks by formulating an effective signal-to-interference-plus-noise ratio (SINR) as well as secrecy capacity under the constraints of the maximum transmit power, the interference threshold, and the hardware impairment level. Furthermore [26], presented a partial relay selection (PRS) protocol to enhance the secrecy performance for cooperative cognitive radio networks (CRNs). For this purpose, the authors investigated the secrecy outage probability (SOP) and the probability of non-zero secrecy capacity (NSC) of the proposed network system. As shown in [27], the problem of designing a good strategy for EH in AF wireless relay systems is considered, and the combination between the wireless power transfer and cooperative jamming (CJ) is studied in [28] for enhancing the physical security in public transportation networks. Full duplex (FD) cognitive radio network, implementing the technique of energy harvesting (EH), is proposed and studied in [29]. And the authors in [30] investigated how to maximize the energy efficiency of the BS while making full use of the relay’s renewable energy and meeting the average throughput requirement. From that point of view, the system performance analysis of the communication cooperative relaying network is the hot research direction in our time.

In this paper, we proposed and investigated Energy Harvesting (EH) based Two-Way Half-Duplex (TWHD) relaying cooperative sensor network using selection combining over block Rayleigh fading channel. Firstly, we proposed the system model with two sources $S_1$, $S_2$, and one intermediate relay $R$. Then, we investigated the system performance in terms of the ergodic capacity (EC) and SER. Finally, all the mathematical analytical expressions are verified by Monte Carlo simulation, and the influence of some main system parameters on the system performance is demonstrated. From the discussions, we can see that the analytical and simulation agree well with each other. The main contribution of this research can be pointed out as the followings:

(1) Energy harvesting based two-way half-duplex relaying cooperative network using selection combining over block Rayleigh fading channel is proposed and investigated
(2) The closed-form of the upper bound EC and exact SER of the model system is derived.
(3) All the results are convinced by Monte Carlo simulation in connection with all primary system parameters.

The rest of this manuscript can be drawn as follows. We provide the system model, the energy and information transfer phases in Section 2. The closed-form expressions of system upper bound EC and SER are derived in Section 3. We introduce the results and some discussions in Section 4. In the last section, some conclusions are proposed.

2. Relaying Network Model

In this section, the energy harvesting based two-way half-duplex relaying sensor cooperative network is drawn in Figure 1. In this system model, sources are denoted as S1 and S2, and the relay is R. We assume that all links between them are available and are block Rayleigh fading channels. The EH and information transformation (IT) for this proposed model system are illustrated in Figure 2. In this protocol, the transmission is divided into blocks of length T, which consists of three-time slots. In the first time slot T/3, the R harvests energy ρP1 from the source node S1, and the source uses the energy (1−ρ)P1 for information transmission to R and S2 (here 0 < ρ < 1: is the power splitting factor). In the second interval time T/3, the R harvests energy ρP2 from the source node S2, and the source S2 uses the energy (1−ρ)P2 for information transmission to R and S1. Finally, the remaining time slot T/3 is used for information transferring from the R to the source nodes S1 and S2 [30–35].

Figure 1. The proposed system model.

Figure 2. EH and IT in the proposed system.
2.1. Energy Harvesting Phase

Let \( S_1 \) transmits the symbol \( x_1 \) in the first phase. The received signal at the relay node \( R \) and source node \( S_2 \) can be expressed, respectively, as

\[
\begin{align*}
y_{1,R}^I &= h_{1,R} x_1 + n_r^I \\
y_{1,2}^I &= h_{1,2} x_1 + n_2^I
\end{align*}
\]  

(1)

where \( E[|x_1|^2] = P_1 \), \( E[\bullet] \) is expectation operator and \( P_1 \) represents the average transmit power at the \( S_1 \). Further, \( n_r^I \) and \( n_2^I \) denote the zero-mean additive white Gaussian noise (AWGN) with variance \( N_0 \) and \( h_{1,R}, h_{2,R} \) are the channel gain of \( S_1-R \) and \( S_2-R \) links, respectively.

The harvested energy at the relay node can be given as

\[
E_h^I = \frac{\eta \rho P_1 |h_{1,R}|^2 T}{3}
\]  

(2)

where \( 0 < \eta \leq 1 \) is energy conversion efficiency and \( 0 < \rho < 1 \) is the power splitting factor.

In the second phase, the source node \( S_2 \) will transmit the symbol \( x_2 \) to the nodes \( R \) and \( S_1 \). Therefore, the received signals at the \( R \) and \( S_1 \) can be expressed, respectively, as

\[
\begin{align*}
y_{2,R}^I &= h_{2,R} x_2 + n_r^I \\
y_{2,1}^I &= h_{2,1} x_2 + n_1^I
\end{align*}
\]  

(3)

where \( E[|x_2|^2] = P_2 \), \( P_2 \) represents the average transmit power at the \( S_2 \). Further, we assume that \( n_r^I \) and \( n_1^I \) are the zero-mean additive white Gaussian noise (AWGN) with variance \( N_0 \).

Similar to the first phase, the total harvested energy at the relay node can be obtained as

\[
E_h = \frac{\eta \rho (P_1 |h_{1,R}|^2 + P_2 |h_{2,R}|^2) T}{3}
\]  

(4)

We assume that the average transmit power from source \( S_1 \) and \( S_2 \) is equal. So, the Equation (4) can be rewritten as

\[
E_h = \frac{\eta \rho (P_1 |h_{1,R}|^2 + P_2 |h_{2,R}|^2) T}{3} = \frac{\eta \rho (|h_{1,R}|^2 + |h_{2,R}|^2) T}{3}
\]  

(5)

where we denote \( P_1 = P_2 = P \).

Therefore, the average transmit power at the relay node can be given as

\[
P_R = \frac{E_h}{(T/3)} = \frac{\eta \rho (|h_{1,R}|^2 + |h_{2,R}|^2) T}{3}
\]  

(6)

2.2. Information Transmission Phase

In the first phase, after doing EH, \( S_1 \) will broadcast the information to the \( R \) node and \( S_2 \) with remaining power \( (1 - \rho)P \). Hence, the received signal at the \( R \) node and \( S_2 \) node can be expressed, respectively, as

\[
\begin{align*}
y_{1,R}^f &= \sqrt{1 - \rho} h_{1,R} x_1 + n_r^f \\
y_{1,2}^f &= h_{1,2} x_1 + n_2^f
\end{align*}
\]  

(7)

where \( h_{1,2} \) is the channel gain of \( S_1-S_2 \) link.
Similar to the first phase, the received signal at the R node and $S_1$ node can be given in the second phase, respectively, as

$$
y_{2,R}^I = \sqrt{1-\rho}h_{2,R}x_2 + n_{1}^I
$$

$$
y_{2,1}^I = h_{2,1}x_2 + n_{1}^I
$$

where $h_{2,1}$ is the channel gain of $S_2$-$S_1$ link.

Finally, in the third phase, the received signal at the source $S_1$ and $S_2$ can be expressed, respectively, as

$$
y_{1}^I = h_{R,1}x_R + n_{1}^{III}
y_{2}^I = h_{R,2}x_R + n_{2}^{III}
$$

where we denote $E[x_R^2] = P_R$. And $h_{R,1}, h_{R,2}$ are the channel gain of $R$-$S_1$ and $R$-$S_2$ links, respectively.

In AF technique, in order to ensure that the transmission power at $R$ is $P_R$, the amplifying coefficient $\chi$ can be chosen as

$$
\chi = \frac{x_R}{y_R} = \frac{P_R}{\sqrt{(1-\rho)[P_1|h_{1,R}|^2 + P_2|h_{2,R}|^2]} + N_0} = \sqrt{\frac{P_R}{(1-\rho)[P_1|h_{1,R}|^2 + P_2|h_{2,R}|^2] + N_0}}
$$

From Equation (9), the received signal at the source $S_1$ can be rewritten as

$$
y_{1}^{III} = h_{R,1}x_R + n_{1}^{III} = h_{R,1}\chi(y_{1,R}^I + y_{2,R}^I) + n_{1}^{III}
$$

where $n_{1}^{III}$ denote the zero-mean additive white Gaussian noise (AWGN) with variance $N_0$.

Replace Equations (7) and (8) into (11); finally, we have

$$
y_{1}^{III} = h_{R,1}\chi\left[\sqrt{1-\rho}h_{1,R}x_1 + \sqrt{1-\rho}h_{2,R}x_2 + n_{1}^I + n_{1}^{III}\right] + n_{1}^{III}
$$

$$
= \chi h_{R,1}h_{1,R}\sqrt{1-\rho}x_1 + h_{R,1}\chi\sqrt{1-\rho}h_{2,R}x_2 + h_{R,1}\chi n_r + n_{1}^{III}
$$

where $n_r = n_1^I + n_1^{III}$ denote the total AWGN at the relay with variance $N_0$.

This signal contains both messages $x_1$ and $x_2$, while the only $x_2$ is the desired signal at $x_1$. Since node $x_1$ perfectly knows its transmitted symbol $x_1$, it can eliminate the corresponding self-interference term $\chi h_{R,1}h_{1,R}\sqrt{1-\rho}x_1$ from $y_{1}^{III}$. Therefore, Equation (12) can be rewritten as

$$
y_{1}^{III} = h_{R,1}\chi\sqrt{1-\rho}h_{2,R}x_2 + h_{R,1}\chi n_r + n_{1}^{III}
$$

From Equation (13), the signal to noise ratio (SNR) of $S_2$-$R$-$S_1$ link can be calculated as

$$
\gamma_{2,1}^{AF} = \frac{E[|signal|^2]}{E[|noise|^2]} = \frac{|h_{R,1}|^2|h_{2,R}|^2P_2\chi^2(1-\rho)}{|h_{R,1}|^2\chi^2N_0 + N_0} = \frac{|h_{R,1}|^2|h_{2,R}|^2P(1-\rho)}{|h_{R,1}|^2N_0 + \frac{N_0}{\chi^2}}
$$

Replace (10) into (14), and after doing some algebra, we have the final form

$$
\gamma_{2,1}^{AF} \approx \frac{\varphi_1 \varphi_2 \psi \rho(1-\rho)}{\eta \psi_1 + (1-\rho)}
$$

where we denote $\psi = \frac{P_2}{N_0} = \frac{P_2}{N_0}, \varphi_1 = |h_{R,1}|^2, \varphi_2 = |h_{2,R}|^2$. 

Sensors 2020, 20, 1165
In the second phase, $S_2$ will transmit the data to $S_1$ directly, from Equation (8) the received signal destination can be given as

$$\gamma_{2,1}^{\text{direct}} = P_2 |h_{2,1}|^2 = \psi \varphi_3$$

where we denote $\varphi_3 = |h_{2,1}|^2$.

Finally, using the selection combining (SC) at the receiver $S_1$, the end to end SNR of AF mode at the source $S_1$ can be obtained as

$$\gamma_{AF} = \max\left[\gamma_{AF}^{\text{direct}}, \gamma_{2,1}'\right] = \max\left[\varphi_1 \varphi_2 \psi \rho (1-\rho), \eta \rho \varphi_1 (1-\rho) \psi \varphi_3\right]$$

### 3. Upper Bound Ergodic Capacity and Exact SER Analysis

#### 3.1. Upper Bound Ergodic Capacity Analysis

The EC of the proposed system can be formulated as the following

$$C = \mathbb{E}\{\log_2(1+\gamma_{AF})\} = \int_0^\infty f_{\gamma_{AF}}(x) \log_2(1+x)dx$$

It is easy to observe that Equation (18) is tough to compute in the closed-form expression. So, we will calculate it in the UPPER bound analysis. From Equation (18), EC in UPPER bound can be given as the following equation

$$C = \mathbb{E}\{\log_2(1+\gamma_{AF})\} \leq C_{UP}$$

where $C_{UP} = \log_2\{1 + \mathbb{E}\{\gamma_{AF}\}\}$.

Here, we have

$$\mathbb{E}\{\gamma_{AF}\} = \int_0^\infty x \times f_{\gamma_{AF}}(x)dx$$

where $f_{\gamma_{AF}}(x) = \frac{\partial F_{\gamma_{AF}}(x)}{\partial x}$.

In order to calculate Equation (20), we have to find $F_{\gamma_{AF}}(x)$. So, combined with Equation (17), $F_{\gamma_{AF}}(x)$ can be given as

$$F_{\gamma_{AF}}(x) = \Pr\{\gamma_{AF} < x\} = \Pr\left(\max\left[\varphi_1 \varphi_2 \psi \rho (1-\rho), \eta \rho \varphi_1 (1-\rho) \psi \varphi_3\right] < x\right)$$

$$= \Pr\left[\varphi_1 \varphi_2 \psi \rho (1-\rho) \varphi_1 (1-\rho) \frac{\eta \rho \varphi_1 (1-\rho)}{\varphi_1 \varphi_2 \psi \rho (1-\rho)} < x\right] \times \Pr(\varphi_3 < x)$$

Firstly, we consider $P_1$

$$P_1 = \Pr\left(\varphi_2 < \frac{x}{\varphi_1 \varphi_2 \psi \rho (1-\rho)}\right) = \Pr\left(\varphi_2 < \frac{x}{\varphi_1 \varphi_2 \psi \rho (1-\rho)}\right)$$

$$= \int_0^\infty x \varphi_2 \left(\frac{x}{\varphi_1 \varphi_2 \psi \rho (1-\rho)}\right) \varphi_1 d\varphi_1$$

$$= \int_0^\infty \varphi_2 \left(\frac{x}{\varphi_1 \varphi_2 \psi \rho (1-\rho)}\right) \varphi_1 d\varphi_1$$

$$= 1 - \frac{\lambda_1}{\lambda_1} \exp\left[-\frac{x}{\lambda_2 \psi (1-\rho)}\right] \times \int_0^\infty \exp\left[-\frac{x}{\lambda_2 \psi (1-\rho)} - \frac{\psi_1}{\lambda_1}\right] d\varphi_1$$

$$= 1 - \frac{\lambda_1}{\lambda_1} \exp\left[-\frac{x}{\lambda_2 \psi (1-\rho)}\right] \times \int_0^\infty \exp\left[-\frac{x}{\lambda_2 \psi (1-\rho)} - \frac{\psi_1}{\lambda_1}\right] d\varphi_1$$
where $\lambda_1, \lambda_2$ are the mean of the random variable (RV) $\varphi_1, \varphi_2$, respectively.

Applying Equation (3.324.1) in [36], Equation (22) can be reformulated as

$$P_1 = 1 - 2 \exp \left[ -\frac{x}{\lambda_2 \psi(1-\rho)} \right] \times \sqrt{\frac{x}{\lambda_1 \lambda_2 \psi \eta \rho}} \times K_1 \left( 2 \sqrt{\frac{x}{\lambda_1 \lambda_2 \psi \eta \rho}} \right)$$ \hspace{1cm} (23)

Secondly, $P_2$ can be obtained by the following equation

$$P_2 = \Pr[\psi \varphi_3 < \gamma \eta] = \Pr\left\{ \varphi_3 < \frac{\gamma \eta}{\psi} \right\} = 1 - \exp \left[ -\frac{\gamma \eta}{\lambda_3 \psi} \right]$$ \hspace{1cm} (24)

where $\lambda_3$ is the mean of RV $\varphi_3$.

Substituting Equations (23) and (24) into (21), we can obtain $F_{A1}(x)$ as followings

$$F_{A1}(x) = \left\{ 1 - \exp \left[ -\frac{x}{\lambda_3 \psi} \right] \right\} \times \left\{ 1 - 2 \exp \left[ -\frac{x}{\lambda_2 \psi(1-\rho)} \right] \times \sqrt{\frac{x}{\lambda_1 \lambda_2 \psi \eta \rho}} \times K_1 \left( 2 \sqrt{\frac{x}{\lambda_1 \lambda_2 \psi \eta \rho}} \right) \right\}$$ \hspace{1cm} (25)

where $K_0(\bullet)$ is the modified Bessel function of the second kind and $v$th order.

Derivate Equation (25) by using the formula $\frac{d}{dx}(x^n K_0(x)) = -x^n K_{v-1}(x)$, we have

$$f_{A1}(x) = \frac{\exp \left[ -\frac{x}{\lambda_2 \psi} \right] \times \left\{ 1 - 2 \exp \left[ -\frac{x}{\lambda_2 \psi(1-\rho)} \right] \times \sqrt{\frac{x}{\lambda_1 \lambda_2 \psi \eta \rho}} \times K_1 \left( 2 \sqrt{\frac{x}{\lambda_1 \lambda_2 \psi \eta \rho}} \right) \right\}}{\lambda_2 \psi(1-\rho)} \times \left\{ 1 - \exp \left[ -\frac{x}{\lambda_3 \psi} \right] \right\} \times K_1 \left( 2 \sqrt{\frac{x}{\lambda_2 \psi(1-\rho)}} \right)$$ \hspace{1cm} (26)

Substituting Equation (26) into (20), we have

$$E\left[ \gamma_{A1}^\varphi \right] = \int_0^\infty x \times \Xi(x) dx + \int_0^\infty x \times \Theta(x) dx$$ \hspace{1cm} (27)

The first term of Equation (27) can be derived as

$$\int_0^\infty x \times \Xi(x) dx = \frac{1}{\lambda_3 \psi} \int_0^\infty x \exp \left[ -\frac{x}{\lambda_3 \psi} \right] dx - \frac{2}{\lambda_3 \psi \sqrt{\lambda_1 \lambda_2 \psi \eta \rho}} \times \int_0^\infty x^{3/2} \exp \left[ -x \left( \frac{1}{\lambda_2 \psi(1-\rho)} + \frac{1}{\lambda_3 \psi} \right) \right] \times K_1 \left( 2 \sqrt{\frac{x}{\lambda_2 \psi(1-\rho)}} \right) dx$$ \hspace{1cm} (28)

where we demote

$$A_1 = \frac{1}{\lambda_3 \psi} \int_0^\infty x \exp \left[ -\frac{x}{\lambda_3 \psi} \right] dx = \lambda_3 \psi$$ \hspace{1cm} (29)
And then applying Equation (6.643,3) in [36], $A_2$ can be reformulated as

\[
A_2 = \frac{2}{\lambda_3} \sqrt{z_1 z_2 \eta \rho} \int_0^\infty x^{3/2} \exp\left\{-\frac{x}{\lambda_2 \psi(1 - \rho)} + \frac{x}{\lambda_3} \right\} \times K_1 \left(2 \sqrt{\frac{x}{\lambda_1 \lambda_2 \eta \rho}}\right) dx
\]

\[
= \frac{2}{\lambda_3} \sqrt{z_1 z_2 \eta \rho} \times \sqrt{\frac{z_1 z_2 \eta \rho}{2}} \times \Gamma(3) \Gamma(2) \exp\left\{\frac{1}{2} \left(2 \frac{z_1 z_2 \eta \rho}{1 - \rho} + z_1 z_2 \eta \rho - 3\right)\right\} \times \frac{1}{\lambda_2 \psi(1 - \rho) + \frac{1}{\lambda_3} \left(\frac{\lambda_3 (1 - \rho)}{2 \lambda_1 \eta \rho (\lambda_3 + \lambda_2 [1 - \rho])}\right)}
\]

(30)

where $\Gamma(\cdot)$ is the Gamma function and $W(\cdot)$ is the Whittaker function.

The second term of Equation (27) can be derived as

\[
\int_0^\infty x \times \Theta(x) dx = \int_0^\infty \left\{1 - \exp\left(-\frac{x}{\lambda_3 \psi}\right)\right\} \times \exp\left[-\frac{x}{\lambda_2 \psi(1 - \rho)}\right] \times \left\{K_0 \left(2 \sqrt{\frac{x}{\lambda_2 \psi(1 - \rho)}}\right)\right\} + \frac{1}{\lambda_2 \psi(1 - \rho)} \times K_1 \left(2 \sqrt{\frac{x}{\lambda_2 \psi(1 - \rho)}}\right) dx
\]

(31)

where we denote

\[
B_1 = \frac{2}{\lambda_2 \psi(1 - \rho)} \sqrt{z_1 z_2 \eta \rho} \int_0^\infty x^{3/2} \exp\left\{-\frac{x}{\lambda_2 \psi(1 - \rho)}\right\} \times K_1 \left(2 \sqrt{\frac{x}{\lambda_1 \lambda_2 \eta \rho}}\right) dx
\]

\[
B_2 = \frac{2}{\lambda_1 \lambda_2 \eta \rho} \int_0^\infty x \exp\left\{-\frac{x}{\lambda_2 \psi(1 - \rho)}\right\} \times K_0 \left(2 \sqrt{\frac{x}{\lambda_1 \lambda_2 \eta \rho}}\right) dx
\]

\[
B_3 = \frac{2}{\lambda_2 \psi(1 - \rho)} \sqrt{z_1 z_2 \eta \rho} \int_0^\infty x^{3/2} \exp\left\{-x \left[\frac{1}{\lambda_2 \psi(1 - \rho)} + \frac{1}{\lambda_3} \right] \right\} \times K_1 \left(2 \sqrt{\frac{x}{\lambda_1 \lambda_2 \eta \rho}}\right) dx
\]

\[
B_4 = \frac{2}{\lambda_1 \lambda_2 \eta \rho} \int_0^\infty x \exp\left\{-x \left[\frac{1}{\lambda_2 \psi(1 - \rho)} + \frac{1}{\lambda_3} \right] \right\} \times K_0 \left(2 \sqrt{\frac{x}{\lambda_1 \lambda_2 \eta \rho}}\right) dx
\]

By applying Equation (6.643, 3) in [36], we can calculate $B_1$, $B_2$, $B_3$, and $B_4$, respectively, as follows:

\[
B_1 = 2 \lambda_2 \psi(1 - \rho) \times \exp\left(\frac{(1 - \rho)}{2 \lambda_1 \eta \rho}\right) \times W_{-2,\frac{1}{2}} \left(\frac{(1 - \rho)}{2 \lambda_1 \eta \rho}\right)
\]

(32)

\[
B_2 = \frac{1}{\lambda_2 \psi(1 - \rho) \sqrt{z_1 z_2 \eta \rho}} \times \exp\left(\frac{(1 - \rho)}{2 \lambda_1 \eta \rho}\right) \times (1 - \rho)^{-3/2} \times W_{-1/2, \frac{1}{2}} \left(\frac{(1 - \rho)}{2 \lambda_1 \eta \rho}\right)
\]

(33)
\[ B_3 = \frac{2}{\lambda_2 \psi(1-p)} \sqrt{\frac{1}{2}} \lambda_2 \psi \rho \Gamma(3) \Gamma(2) \times \exp \left\{ -\frac{1}{2} \left( \frac{1}{2} + \frac{1}{\lambda_2 \psi + 1} \right) + \frac{1}{\lambda_2 \psi} \right\} \times W_{-2, \frac{\rho}{\lambda_2 \psi}} \left( \frac{1}{2} \frac{1}{\lambda_2 \psi + 1} \right) \times W_{-2, \frac{\rho}{\lambda_2 \psi}} \left( \frac{1}{2} \frac{1}{\lambda_2 \psi + 1} \right) \] \]

(34)

\[ B_4 = \frac{2}{\lambda_1 \lambda_2 \psi \rho} \times \sqrt{\frac{1}{2}} \lambda_1 \lambda_2 \psi \rho \times \exp \left\{ -\frac{1}{2} \left( \frac{1}{2} + \frac{1}{\lambda_1 \lambda_2 \psi + 1} \right) + \frac{1}{\lambda_1 \lambda_2 \psi} \right\} \times W_{-2, \frac{\rho}{\lambda_1 \lambda_2 \psi}} \left( \frac{1}{2} \frac{1}{\lambda_1 \lambda_2 \psi + 1} \right) \times W_{-2, \frac{\rho}{\lambda_1 \lambda_2 \psi}} \left( \frac{1}{2} \frac{1}{\lambda_1 \lambda_2 \psi + 1} \right) \] \]

(35)

\[ C_{\text{upp}} = \log_2 \left[ 1 + \lambda_3 \psi - \frac{2\lambda_2 \psi}{\lambda_1 \lambda_2 \psi + 1} \times \exp \left\{ -\frac{1}{2} \left( \frac{1}{2} + \frac{1}{\lambda_1 \lambda_2 \psi + 1} \right) + \frac{1}{\lambda_1 \lambda_2 \psi} \right\} \times W_{-2, \frac{\rho}{\lambda_1 \lambda_2 \psi}} \left( \frac{1}{2} \frac{1}{\lambda_1 \lambda_2 \psi + 1} \right) \times W_{-2, \frac{\rho}{\lambda_1 \lambda_2 \psi}} \left( \frac{1}{2} \frac{1}{\lambda_1 \lambda_2 \psi + 1} \right) \right] - \frac{2\lambda_2 \psi}{\lambda_1 \lambda_2 \psi + 1} \times \frac{1}{\lambda_1 \lambda_2 \psi + 1} \times \exp \left\{ -\frac{1}{2} \left( \frac{1}{2} + \frac{1}{\lambda_1 \lambda_2 \psi + 1} \right) + \frac{1}{\lambda_1 \lambda_2 \psi} \right\} \times W_{-2, \frac{\rho}{\lambda_1 \lambda_2 \psi}} \left( \frac{1}{2} \frac{1}{\lambda_1 \lambda_2 \psi + 1} \right) \times W_{-2, \frac{\rho}{\lambda_1 \lambda_2 \psi}} \left( \frac{1}{2} \frac{1}{\lambda_1 \lambda_2 \psi + 1} \right) \] \]

(36)

where \( W(\bullet) \) is the Whittaker function which can be defined in [36].

3.2. SER Analysis

In this section, we obtain new expressions for the SER at the destination. We first consider the outage probability, which was obtained in [31]. Thus, we have

\[ \text{SER}_1 = \mathbb{E}\left[ aQ\left( \sqrt{2b}\sqrt{\frac{A_F}{\gamma_{\text{req}}}} \right) \right] \] \]

(37)

\[ Q(t) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} e^{-x^2/2} dx \] is the Gaussian Q-function, while \( a \) and \( b \) are constants, which are specific for modulation type. \((a, b) = (1, 1)\) for binary phase-shift keying (BPSK) and \((a, b) = (1, 2)\) for Quadrature Phase Shift Keying (QPSK). As a result, before obtaining the SER performance, the distribution function of \( \gamma_{\text{req}} \) is expected. Then, we begin rewriting the SER expression given in Equation (37) directly in terms of outage probability at the source \( S_1 \) by using integration, as follows

\[ \text{SER}_1 = \frac{a}{\sqrt{2\pi}} \int_{0}^{\infty} e^{-bx} F_{\gamma_{\text{req}}} (x) dx \] \]

(38)

Substituting Equation (25) into (38), we have

\[ \text{SER}_1 = \frac{a}{\sqrt{2\pi}} \int_{0}^{\infty} e^{-bx} \left\{ \left[ 1 - \exp \left( -\frac{x}{\lambda_3 \psi} \right) \right] \left[ 1 - 2 \exp \left( -\frac{x}{\lambda_2 \psi + 1} \right) \right] \times \sqrt{\frac{x}{\lambda_2 \psi + 1}} \times K_1 \left( 2 \sqrt{\frac{x}{\lambda_2 \psi + 1}} \right) \right\} dx \]

(39)

\[ = l_1 - l_2 - l_3 + l_4 \]
where we denote

\[ I_1 = \frac{a\sqrt{b} \Gamma}{2\sqrt{\pi}} \int_0^\infty \frac{e^{-bx}}{\sqrt{x}} \, dx, \quad I_2 = \frac{a\sqrt{b} \Gamma}{2\sqrt{\pi}} \int_0^\infty \exp\left[-x\left(b + \frac{1}{\lambda_2\psi}\right)\right] \, dx \]

Apply Equation (3.361,2) in [36], \( I_1 \) and \( I_2 \) can be obtained as, respectively

\[ I_1 = \frac{a}{2} \]

and

\[ I_2 = \frac{a}{2\sqrt{1 + \frac{1}{\lambda_3\psi}}} \]

Moreover, \( I_3 \) and \( I_4 \) can be denoted as

\[ I_3 = \frac{a\sqrt{b} \Gamma}{\sqrt{\pi\lambda_1\lambda_2\eta\rho\psi}} \int_0^\infty \exp\left[-x\left(b + \frac{1}{\lambda_2\psi(1-\rho)}\right)\right] \times K_1\left(2\sqrt{\frac{x}{\lambda_2\psi\rho\lambda_1}}\right) \, dx \]

and

\[ I_4 = \frac{a\sqrt{b} \Gamma}{\sqrt{\pi\lambda_1\lambda_2\eta\rho\psi}} \int_0^\infty \exp\left[-x\left(b + \frac{1}{\lambda_2\psi(1-\rho)} + \frac{1}{\lambda_3\psi}\right)\right] \times K_1\left(2\sqrt{\frac{x}{\lambda_2\psi\eta\rho\lambda_1}}\right) \, dx \]

Applying Equation (6.614,4) in [36], \( I_3 \) and \( I_4 \) can be claimed as, respectively

\[ I_3 = \frac{a\sqrt{b} \Gamma}{2\sqrt{\pi}} \times \frac{\exp\left(2\lambda_1\lambda_2\psi\rho\psi \left\lbrack b + \frac{1}{\lambda_2\psi(1-\rho)} \right\rbrack\right)}{2\sqrt{b + \frac{1}{\lambda_2\psi(1-\rho)}}} \times \Gamma\left(\frac{3}{2}\right) \Gamma\left(\frac{1}{2}\right) \times W_{-1,\frac{1}{2}}\left(\lambda_1\lambda_2\psi\rho\psi \left\lbrack b + \frac{1}{\lambda_2\psi(1-\rho)} \right\rbrack\right) \]

\[ I_4 = \frac{a\sqrt{b} \Gamma}{2\sqrt{\pi}} \times \frac{\exp\left(2\lambda_1\lambda_2\psi\rho\psi \left\lbrack b + \frac{1}{\lambda_2\psi(1-\rho)} + \frac{1}{\lambda_3\psi}\right\rbrack\right)}{2\sqrt{\left(b + \frac{1}{\lambda_2\psi(1-\rho)} + \frac{1}{\lambda_3\psi}\right)}} \times \Gamma\left(\frac{3}{2}\right) \Gamma\left(\frac{1}{2}\right) \times W_{-1,\frac{1}{2}}\left(\lambda_1\lambda_2\psi\rho\psi \left\lbrack b + \frac{1}{\lambda_2\psi(1-\rho)} + \frac{1}{\lambda_3\psi}\right\rbrack\right) \]

where \( \Gamma(\bullet) \) is the Gamma function and \( W(\bullet) \) is the Whittaker function.

Finally, substituting Equations (40)–(43) into (39), SER at the source \( S_1 \) can be obtained as

\[ SER_1 = \frac{a}{2} - \frac{a\sqrt{b} \Gamma}{2\sqrt{\pi}} \times \frac{\exp\left(2\lambda_1\lambda_2\psi\rho\psi \left\lbrack b + \frac{1}{\lambda_2\psi(1-\rho)} \right\rbrack\right)}{2\sqrt{b + \frac{1}{\lambda_2\psi(1-\rho)}}} \times \Gamma\left(\frac{3}{2}\right) \Gamma\left(\frac{1}{2}\right) \times W_{-1,\frac{1}{2}}\left(\lambda_1\lambda_2\psi\rho\psi \left\lbrack b + \frac{1}{\lambda_2\psi(1-\rho)} \right\rbrack\right) \]

\[ + \frac{a\sqrt{b} \Gamma}{2\sqrt{\pi}} \times \frac{\exp\left(2\lambda_1\lambda_2\psi\rho\psi \left\lbrack b + \frac{1}{\lambda_2\psi(1-\rho)} + \frac{1}{\lambda_3\psi}\right\rbrack\right)}{2\sqrt{\left(b + \frac{1}{\lambda_2\psi(1-\rho)} + \frac{1}{\lambda_3\psi}\right)}} \times \Gamma\left(\frac{3}{2}\right) \Gamma\left(\frac{1}{2}\right) \times W_{-1,\frac{1}{2}}\left(\lambda_1\lambda_2\psi\rho\psi \left\lbrack b + \frac{1}{\lambda_2\psi(1-\rho)} + \frac{1}{\lambda_3\psi}\right\rbrack\right) \]
4. Numerical Results and Discussion

In this section, we present numerical results to demonstrate the system performance of the proposed system network in the above section. The correctness of the analytical analysis in the above section is verified by the Monte Carlo simulation as in [25–29,36–44].

In this section, we investigate the impact of $\psi$ on the system performance of the proposed system in cases with and without the direct link between the $S_1$ and $S_2$ nodes. The Figure 3 shows the system EC versus $\psi$ in the presence of the direct link between the $S_1$ and $S_2$ sources. In Figure 3, we set some primary system parameters as $\eta = 0.8$, $\lambda_1 = 5$, $\lambda_2 = \lambda_4 = 10$, $\lambda_3 = 2$, $\varphi = 0.5$, and 0.85. In this simulation, we consider both the exact and upper bond EC in the influence of $\psi$ as shown in Figure 3. From Figure 3, we can state that both the exact and upper bond system EC rise while we vary $\psi$ from 10 dB to 10 dB and the exact EC is higher than the upper bond system EC with all $\psi$ values. Moreover, the analytical expression of the exact and upper bond system EC in the above section is verified by the simulation results using Monte Carlo Simulation. Furthermore, the comparison system EC in cases with and without a direct link between the sources $S_1$ and $S_2$ is illustrated in Figure 4 with the primary system parameters as $\eta = 0.5$ and 0.85, respectively. In the same way with the above case, the system EC significantly increases with rising $\psi$ from 10 dB to 10 dB in both cases with and without a direct link between the sources $S_1$ and $S_2$ as in Figure 4. In addition, the system EC in the case with a direct link is better than in the case without a direct link between two sources. It can be observed that the direct link can lead to more useful information transmission in the proposed system. In the model system with the direct link, system has two way to transfer the information as via helping relay and direct link. With two way of information transmission via relay and direct link, this case is effective in information transferring in comparison with the case only with helping of the relay as in [45]. Further, the analytical and the simulation results match well for all possible values of $\psi$ as shown in Figure 4.

In order to further observe the effect of power splitting coefficient $\varphi$ on the exact and upper bond system EC, Figure 5 shows the exact and upper bond system EC versus $\varphi$ with the main system parameters as the follows $\eta = 0.8$, $\lambda_1 = 5$, $\lambda_2 = \lambda_4 = 10$, $\lambda_3 = 2$, $\psi = 5$, and 10 dB, respectively. In this case, we vary the power splitting coefficient $\varphi$ from 0 to 1. From the result, we can see that the exact and upper bond system EC increases significantly to the optimal values while $\varphi$ increases to 0.4, and after that falls up from the optimal values with the rising of $\varphi$ to 1. This is the case because more energy used for the harvesting energy process can lead to an increase of the system EC. Still, the over-harvesting energy process can cause less information transmission and lead to the falling of the system EC as shown in Figure 5. In addition, the difference of the upper and exact maximum ergodic capacity as shown in Figure 3 with $\varphi = 0.5$ is $0.4681 \text{ bps/Hz (} \approx 9.5\%)$, $0.4681 \text{ bps/Hz (} \approx 9.5\%)$ and $\varphi = 0.85$ is $0.3927 \text{ bps/Hz (} \approx 9.1\%)$; and in Figure 5, the difference of the upper and exact maximum ergodic capacity with $\psi = 5\text{dB}$ is $0.4398 \text{ bps/Hz (} \approx 12.7\%)$ and with $\psi = 10\text{dB}$ is $0.51 \text{ bps/Hz (} \approx 10.2\%)$.

Furthermore, the comparison of the system EC of the cases with and without a direct link between the sources $S_1$ and $S_2$ is drawn in Figure 6 with $\eta = 0.5$ and 0.85, respectively. As shown in Figure 6, the system EC in the case with the presence of the direct link is better than the case without in connection with the better information and energy transmission processes with the direct link between the sources. In both Figures 5 and 6, the simulation and the analytical values are the same with all values of $\varphi$ to confirm the analytical analysis in the above section.
Figure 3. EC versus $\psi$.

Figure 4. The comparison EC versus $\psi$.

Figure 5. EC versus $\rho$. 
Finally, Figures 7 and 8 show the effect of the $\psi$ and $\varrho$ on the system SER, respectively. Here, we set the main system parameters as $\eta = 0.8$, $\lambda_1 = 5$, $\lambda_2 = \lambda_3 = 2$, $\psi = 10$ dB for Figure 8 and $\varrho = 0.5$ for Figure 7, respectively. Moreover, the system SER significantly falls while the $\psi$ varies from $-10$ dB to 10 dB as shown in Figure 7. From the results in Figure 8, it can be seen that the system SER decreases with $\varrho$ varies from 0.1 to 0.5, and after that increases with $\varrho$ from 0.5 to 1. The optimal value of system SER can be obtained with $\varrho$ from 0.4 to 0.6. It can be observed from Figures 6 and 7 that the analytical results have an agreement to the simulations for both cases to verify the correctness of the above analytical section.
5. Conclusions

In this paper, we investigated the EH Based TWHD relaying sensor network system using selection combining over block Rayleigh fading channel. In this model, we propose the direct link between two sources for improving the system performance. For the system performance analysis, we investigate and derived the closed-form of the upper bound EC and the exact form of the SER. By using the Monte Carlo simulation, the correctness of the research results is verified in the influence of the main system parameters. From the discussions, we can see that the analytical and simulation agree well with each other. This research can be considered as a novel recommendation for a communication cooperative relaying sensor network.

Author Contributions: Methodology, P.T.T., T.N.N. and L.S.; software, T.N.N., P.T.T. and T.T.T.; validation, T.N.N., P.T.T. and T.T.T.; writing—original draft preparation, M.T.; writing—review and editing, M.T. All authors have read and agreed to the published version of the manuscript.

Funding: The research was supported by the Czech Ministry of Education, Youth and Sports from the Large Infrastructures for Research, Experimental Development and Innovations project, IT4Innovations National Supercomputing Center—LM2015070.

Conflicts of Interest: The authors declare no conflict of interest.

References

1. Bi, S.; Ho, C.K.; Zhang, R. Wireless powered communication: Opportunities and challenges. *IEEE Commun. Mag.* 2015, 53, 117–125. [CrossRef]
2. Niyato, D.; Kim, D.I.; Maso, M.; Han, Z. Wireless Powered Communication Networks: Research Directions and Technological Approaches. *IEEE Wirel. Commun.* 2017, 24, 2–11. [CrossRef]
3. Yu, H.; Lee, H.; Jeon, H. What is 5G? Emerging 5G Mobile Services and Network Requirements. *Sustainability* 2017, 9, 1848. [CrossRef]
4. Salem, A.; Khairi, A.H.; Khaled, M.R. Physical Layer Security with RF Energy Harvesting in AF Multi-Antenna Relaying Networks. *IEEE Trans. Commun.* 2016, 64, 3025–3038. [CrossRef]
5. Liu, W.; Zhou, X.; Durrani, S.; Popovski, P. Secure Communication with a Wireless-Powered Friendly Jammer. *IEEE Trans. Wirel. Commun.* 2016, 15, 401–415. [CrossRef]
6. Varshney, L.R. Transporting Information Energy Simultaneously. In Proceedings of the 2008 IEEE International Symposium on Information Theory, Toronto, ON, Canada, 6–11 July 2008. [CrossRef]
7. Zhou, X.; Zhang, R.; Ho, C.K. Wireless Information and Power Transfer: Architecture Design and Rate-Energy Tradeoff. *IEEE Trans. Commun.* 2013, 61, 4754–4767. [CrossRef]
8. Liu, L.; Zhang, R.; Chua, C.-K. Wireless Information Transfer with Opportunistic Energy Harvesting. *IEEE Trans. Wirel. Commun.* **2013**, *12*, 288–300. [CrossRef]
9. Xiang, Z.; Tao, M. Robust Beamforming for Wireless Information and Power Transmission. *IEEE Wirel. Commun. Lett.* **2012**, *1*, 372–375. [CrossRef]
10. Bhargav, M.; Mehta, N.B. Voluntary Energy Harvesting Relays and Selection in Cooperative Wireless Networks. *IEEE Trans. Wirel. Commun.* **2010**, *9*, 3543–3553. [CrossRef]
11. Nasir, A.A.; Zhou, X.; Durrani, S.; Kennedy, R.A. Relaying Protocols for Wireless Energy Harvesting and Information Processing. *IEEE Trans. Wirel. Commun.* **2013**, *12*, 3622–3636. [CrossRef]
12. Grover, P.; Sahai, A. Shannon Meets Tesla: Wireless Information and Power Transfer. In *Proceedings of the 2010 IEEE International Symposium on Information Theory*, Austin, TX, USA, 13–18 June 2010. [CrossRef]
13. Huang, K.; Lau, V.K.N. Enabling Wireless Power Transfer in Cellular Networks: Architecture, Modeling and Deployment. *IEEE Trans. Wirel. Commun.* **2014**, *13*, 902–912. [CrossRef]
14. Nguyen, T.N.; Minh, T.; Long, N.T.; Hung, D.H.; Voznak, M. Multisource Power Splitting Energy Harvesting Relaying Network in Half-Duplex System over Block Rayleigh Fading Channel: System Performance Analysis. *Electronics* **2019**, *8*, 67. [CrossRef]
15. Shi, Q.; Liu, L.; Xu, W.; Zhang, R. Joint Transmit Beamforming and Receive Power Splitting for MISO SWIPT Systems. *IEEE Trans. Wirel. Commun.* **2014**, *13*, 3269–3280. [CrossRef]
16. Zhang, R.; Ho, C.K. MIMO Broadcasting for Simultaneous Wireless Information and Power Transfer. *IEEE Trans. Wirel. Commun.* **2013**, *12*, 1989–2001. [CrossRef]
17. Ju, H.; Zhang, R. Throughput Maximization in Wireless Powered Communication Networks. *IEEE Trans. Wirel. Commun.* **2014**, *13*, 418–428. [CrossRef]
18. Krikidis, I.; Timotheou, S.; Sasaki, S. RF Energy Transfer for Cooperative Networks: Data Relaying or Energy Harvesting? *IEEE Commun. Lett.* **2012**, *16*, 1772–1775. [CrossRef]
19. Michalopoulos, D.S.; Suraweera, H.A.; Scholer, R. Relay Selection for Simultaneous Information Transmission and Wireless Energy Transfer: A Tradeoff Perspective. *IEEE J. Sel. Areas Commun.* **2015**, *1*. [CrossRef]
20. Park, J.; Clerckx, B. Joint Wireless Information and Energy Transfer in a Two-User MIMO Interference Channel. *IEEE Trans. Wirel. Commun.* **2013**, *12*, 4210–4221. [CrossRef]
21. Park, J.; Clerckx, B. Joint Wireless Information and Energy Transfer with Reduced Feedback in MIMO Interference Channels. *IEEE J. Sel. Areas Commun.* **2015**, *1*. [CrossRef]
22. Ding, Z.; Perlaza, S.M.; Esnaola, I.; Poor, H.V. Power Allocation Strategies in Energy Harvesting Wireless Cooperative Networks. *IEEE Trans. Wirel. Commun.* **2014**, *13*, 846–860. [CrossRef]
23. Chen, Z.; Xia, B.; Liu, H. Wireless Information and Power Transfer in Two-way Amplify-and-forward Relaying Channels. In *Proceedings of the 2014 IEEE Global Conference on Signal and Information Processing (GlobalSIP)*, Atlanta, GA, USA, 3–5 December 2014. [CrossRef]
24. Krikidis, I.; Sasaki, S.; Timotheou, S.; Ding, Z. A Low Complexity Antenna Switching for Joint Wireless Information and Energy Transfer in MIMO Relay Channels. *IEEE Trans. Commun.* **2014**, *62*, 1577–1587. [CrossRef]
25. Tin, P.T.; Hung, D.T.; Nguyen, T.; Duy, T.; Voznak, M. Secrecy Performance Enhancement for Underlay Cognitive Radio Networks Employing Cooperative Multi-Hop Transmission with and without Presence of Hardware Impairments. *Entropy* **2019**, *21*, 217. [CrossRef]
26. Tran, H.D.; Tran, D.T.; Choi, S.G. Secrecy Performance of a Generalized Partial Relay Selection Protocol in Underlay Cognitive Networks. *Int. J. Commun. Syst.* **2018**, *31*. [CrossRef]
27. Nguyen, T.L.N.; Shin, Y. Performance Analysis for Energy Harvesting Based Wireless Relay Systems. In *Proceedings of the 2019 IEEE VTS Asia Pacific Wireless Communications Symposium (APWCS)*, Singapore, 28–30 August 2019. [CrossRef]
28. Gui, L.; He, B.; Zhou, X.; Yu, C.; Shu, F.; Li, J. Energy-Efficient Wireless Powered Secure Transmission with Cooperative Jamming for Public Transportation. *IEEE Trans. Green Commun. Netw.* **2019**, *3*, 876–885. [CrossRef]
29. Bhowmick, A.; Chatterjee, A.; Verma, T. Performance of DF Relaying in an Energy Harvesting Full Duplex Cognitive Radio Network. In *Proceedings of the 2019 International Conference on Vision towards Emerging Trends in Communication and Networking (ViTECoN)*, Vellore, India, 30–31 March 2019. [CrossRef]
30. Zhao, M.; Zhao, J.; Zhou, W.; Zhu, J.; Zhang, S. Energy Efficiency Optimization in Relay-assisted Networks with Energy Harvesting Relay Constraints. *China Commun.* **2015**, *12*, 84–94. [CrossRef]
31. Nguyen, T.N.; Minh, Q.; Hoang, T.; Tran, P.T.; Voznak, M. Energy Harvesting over Rician Fading Channel: A Performance Analysis for Half-Duplex Bidirectional Sensor Networks under Hardware Impairments. *Sensors* **2018**, *18*, 1781. [CrossRef]

32. Bhatnagar, M.R. On the Capacity of Decode-and-Forward Relaying over Rician Fading Channels. *IEEE Commun. Lett.* **2013**, *17*, 1100–1103. [CrossRef]

33. Nguyen, T.N.; Minh TH, Q.; Tran, P.T.; Voznak, M.; Duy, T.T.; Nguyen, T.L.; Tin, P.T. Performance Enhancement for Energy Harvesting Based Two-Way Relay Protocols in Wireless Ad-hoc Networks with Partial and Full Relay Selection Methods. *Ad Hoc Netw.* **2019**, *84*, 178–187. [CrossRef]

34. Luo, S.; Zhang, R.; Lim, T.J. Optimal save-then-transmit protocol for energy harvesting wireless transmitters. *IEEE Trans. Wirel. Commun.* **2013**, *12*, 1196–1207. [CrossRef]

35. Nguyen, T.N.; Minh TH, Q.; Tran, P.T.; Voznak, M. Adaptive Energy Harvesting Relaying Protocol for Two-Way Half Duplex System Network over Rician Fading Channel. *Wirel. Commun. Mob. Comput.* **2018**, *2018*, 7693016. [CrossRef]

36. Gradshteyn, I.S.; Ryzhik, I.M. *Table of Integrals, Series, and Products*; Elsevier: San Diego, CA, USA, 2015.

37. McKay, M.R.; Grant, A.J.; Collings, I.B. Performance analysis of MIMO-MRC in double-correlated Rayleigh environments. *IEEE Trans. Commun.* **2007**, *55*, 497–507. [CrossRef]

38. Chu, Z.; Zhou, F.; Zhu, Z.; Hu, R.Q.; Xiao, P. Wireless Powered Sensor Networks for Internet of Things: Maximum Throughput and Optimal Power Allocation. *IEEE Internet Things J.* **2018**, *5*, 310–321. [CrossRef]

39. Wang, C.-X.; Haider, F.; Gao, X.; You, X.-H.; Yang, Y.; Yuan, D.; Aggoune, H.; Haas, H.; Fletcher, S.; Hepsaydir, E. Cellular Architecture and Key Technologies for 5G Wireless Communication Networks. *IEEE Commun. Mag.* **2014**, *52*, 122–130. [CrossRef]

40. Valenta, C.R.; Durgin, G.D. Harvesting wireless power: Survey of energy-harvester conversion efficiency in far-field, wireless power transfer systems. *IEEE Microw. Mag.* **2014**, *15*, 108–120.

41. Louie, R.H.Y.; Li, Y.; Vucetic, B. Practical physical layer network coding for two-way relay channels: Performance analysis and comparison. *IEEE Trans. Wirel. Commun.* **2010**, *9*, 764–777. [CrossRef]

42. Phan, V.D.; Nguyen, T.N.; Tran, M.; Trang, T.T.; Voznak, M.; Ha, D.H.; Nguyen, T.L. Power Beacon-Assisted Energy Harvesting in a Half-Duplex Communication Network under Co-Channel Interference over a Rayleigh Fading Environment: Energy Efficiency and Outage Probability Analysis. *Energies* **2019**, *12*, 2579. [CrossRef]

43. Nguyen, T.N.; Tran, M.; Ha, D.H.; Trang, T.T.; Voznak, M. Multi-Source in DF Cooperative Networks with PSR protocol Based Full-Duplex Energy Harvesting over Rayleigh Fading Channel: Performance Analysis. *Proc. Est. Acad. Sci.* **2019**, *68*, 111–123. [CrossRef]

44. Nguyen, T.N.; Tran, M.; Ha, D.H.; Nguyen, T.L.; Voznak, M. Energy harvesting based two-way full-duplex relaying network over Rician fading environment: Performance analysis. *Proc. Est. Acad. Sci.* **2019**, *68*, 111–123. [CrossRef]

45. Li, L.; Cimini, L.J.; Xia, X.G. Impact of Direct Link on Outage of Cooperative Full-Duplex Relaying. In Proceedings of the 2015 49th Annual Conference on Information Sciences and Systems (CISS), Baltimore, MD, USA, 18–20 March 2015. [CrossRef]

© 2020 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses/by/4.0/).