Fluorescence enhancement factors on optical antennas: enlarging the experimental values without changing the antenna design

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Abstract

Plasmonic antennas offer promising opportunities to control the emission of quantum objects. As a consequence, the fluorescence enhancement factor is widely used as a figure of merit for a practical antenna realization. However, the fluorescence enhancement factor is not an intrinsic property of the antenna. It critically depends on several parameters, some of which are often disregarded. In this contribution, I explore the influence of the setup collection efficiency, emitter’s quantum yield and excitation intensity. Improperly setting these parameters may significantly alter the enhancement values, leading to potential misinterpretations. The discussion is illustrated by an antenna example of a nanoaperture surrounded by plasmonic corrugations.

1 Introduction

Plasmonic antennas are receiving a large interest to interface light with nanoscale quantum emitters on dimensions much beyond the optical wavelength [1, 2]. Recent developments involve squeezing light into nanoscale volumes [3], enhancing the excitation and emission rate of individual emitters [4, 5, 6, 7, 8], tuning the luminescence spectrum [9, 10], polarization [11] and directivity properties [12, 13, 14, 15, 16]. Several plasmonic systems are being investigated to enhance the luminescence emission of fluorescent molecules or quantum dots, such as metallic nanoparticles [4, 5, 17, 18, 19, 20], core-shell particles [21], thin films [22, 23], nanoantennas [6, 7, 15, 24], nanowires [16], nanoporous gold [25], nanopockets [26], metallic gratings [27], nanoaperture arrays [28], and single nanoapertures [29, 30]. A general review on surface-enhanced fluorescence can be found in reference [31].

A natural question while performing experiments on nanoantenna-enhanced luminescence deals with the quantification of the luminescence enhancement factor $\eta_F$, which is commonly defined as the ratio of the detected radiation power per emitter with the antenna to the reference radiation power per emitter without the antenna. $\eta_F$ determines how many extra photons are detected for each emitter.
thanks to the use of the optical antenna. It is well known that this factor critically depends on several parameters: the antenna material and geometry, its spectral resonance and overlap with the emitter’s absorption and luminescence spectra, as well as the emitter’s orientation and location respective to the antenna [32]. These many parameters often hide the influence of other parameters: the collection efficiency used in the experiments, the emitter’s quantum yield in the absence of the antenna, and the excitation intensity respective to the saturation process. These last three parameters are more technically oriented, and depend on the specific experimental implementation. Therefore, they have received less attention from theoretical investigations. However, as I will show below, these parameters have a major influence on the measured values of the luminescence enhancement factor. Improperly setting these parameters may significantly alter the value found for the luminescence enhancement factor, leading to potential experimental pitfalls.

In this contribution, I explore the influence of the collection efficiency, molecular quantum yield and excitation intensity on the fluorescence enhancement factor. Several rules are derived to maximize the enhancement factor by tuning the experimental conditions without affecting the antenna’s design. Using the fluorescence enhancement factor as a figure of merit to compare between different antenna designs has to be done with caution. Analytical formulas are illustrated by a practical antenna example made of a single nanoaperture surrounded by five shallow grooves in a gold film (Figure 1). This optical antenna can significantly enhance the fluorescence count rates per molecule and control the emission directivity, as demonstrated recently [33]. Very much in the spirit of the review in [34] about the comparison between experiments and numerical simulations, I hope that this article may initiate some reflection, and avoid any misleading interpretation.

2 Designing the experiment to maximize the fluorescence enhancement factor

A loophole in any measurement of the luminescence enhancement factor deals with the normalization of the detected signal per emitter. This can be done by performing experiments on single molecules directly [4, 5, 7], by surface normalization [25, 28], or by calibrating the number of emitters with fluorescence correlation spectroscopy [29, 30]. Hereafter, I consider that this normalization issue is resolved, and that a reliable value for the detected radiated power per emitter can be obtained. I also assume that the signal per emitter has been averaged over several positions and dipole orientations. The aim of this article is to focus on the influence of experimental parameters on the measured values for the fluorescence enhancement factor $\eta_F$. 
2.1 Theoretical background: fluorescence count rate per molecule

Throughout this article, the quantum emitter is modelled by a two energy levels system. $k_r$ and $k_{nr}$ are the rate constants for radiative and non-radiative transitions from the excited singlet state to the ground state. The total deexcitation rate from the excited singlet state is noted as $k_{tot} = k_r + k_{nr}$, which is the inverse of the excited state lifetime $\tau$. $\phi = k_r / k_{tot} = k_r / (k_r + k_{nr})$ is the quantum yield. $\sigma I_e$ is the excitation rate, where $\sigma$ denotes the excitation cross-section and $I_e$ the excitation intensity. Under steady-state conditions, the fluorescence count rate per molecule $CRM$ is given by

$$CRM = \kappa \phi \frac{\sigma I_e}{1 + I_e / I_s}. \quad (1)$$

We note $\kappa$ the light collection efficiency, and $I_s = k_{tot} / \sigma$ the saturation intensity.

Equation (1) takes two limits for the extreme regimes of weak excitation ($I_e \ll I_s$) and fluorescence
saturation \((I_e \gg I_s)\). In the weak excitation regime, the CRM reduces to
\[
CRM = \kappa \phi \sigma I_e \quad (I_e \ll I_s)
\]
which indicates that the fluorescence rate per molecule is proportional to the collection efficiency, the quantum yield, and the excitation intensity. This expression appears to be the one commonly used in fluorescence spectroscopy and microscopy applied to the life sciences [36].

In the saturation regime \(I_e \gg I_s\), Eq. (1) reduces to
\[
CRM = \kappa \phi \sigma I_s = \kappa k_r \quad (I_e \gg I_s)
\]
which indicates that the fluorescence rate per molecule at saturation is determined only by the radiative rate and the collection efficiency, and is of course independent on the excitation rate. This expression is generally used for single-photon sources used for quantum communication purposes, such as quantum cryptography [37, 38].

2.2 Excitation intensity

From Eq. (1), it is apparent that the detected fluorescence rate per emitter – hence the fluorescence enhancement factor – bears a complex dependence upon the excitation intensity \(I_e\). In the weak excitation regime (below the transition to saturation), the CRM is linearly proportional with \(I_e\), and the fluorescence enhancement factor \(\eta_F\) can therefore be expressed as
\[
\eta_F = \frac{CRM^*}{CRM} = \frac{\kappa^* \phi^* \sigma^* I_e^*}{\kappa \phi \sigma I_e} \quad (I_e \ll I_s).
\]
The superscript * denotes the presence of the antenna. In the weak excitation regime, the fluorescence enhancement factor is the product of the enhancements in the collection efficiency, the quantum yield and the excitation intensity (here we assume that the nanoantenna does not modify significantly the fluorophore’s absorption cross section: \(\sigma^* = \sigma\)).

Equation (4) can be rewritten in a slightly different manner to introduce the gains in the radiative rate \(k_r^*/k_r\) and the total fluorescence lifetime reduction \(k_{tot}^*/k_{tot}\):
\[
\eta_F = \frac{\kappa^* \phi^* \sigma^* I_e^*}{\kappa \phi \sigma I_e} = \frac{\kappa^* \phi^* \sigma^* I_e^*}{\kappa \phi \sigma I_e} \quad (I_e \ll I_s).
\]
This equation shows that the fluorescence enhancement factor is proportional to the gains in the radiative rates \(k_r\), and inversely proportional to the total deexcitation rates \(k_{tot}\). Since \(k_{tot}^*/k_{tot} = \tau/\tau^*\) is also the reduction in the fluorescence lifetimes, a strong reduction in the fluorescence lifetimes (sometimes also referred to as Purcell factor) is actually detrimental to the fluorescence enhancement factor. Clearly, the fluorescence lifetimes reduction (Purcell factor) must not be confused with the fluorescence count rate enhancement (see also the discussion in [39]). Observing a strong lifetime
reduction due to the nanoantenna can be related to an increase in the non-radiative transition rate $k_{nr}$, mostly related to ohmic losses. This is the so-called quenching effect, which is certainly not related to any increase in the fluorescence count rate per emitter.

In the saturation regime, it is evident from Eq. (3) that the fluorescence enhancement factor at saturation depends only on the gains in collection efficiency and radiative rate:

$$\eta_F = \frac{\kappa^*}{\kappa^* k_r} \quad (I_e \gg I_s)$$

Interestingly, at saturation of the fluorescence process, the fluorescence enhancement is found independent on the non-radiative transition rate $k_{nr}$, which means that metal quenching might not be an issue in this particular configuration. At saturation, the sole figure of merit is the ability of the emitter–nanoantenna system to radiate photons into the photonic modes used for detection, which is quantified by $\kappa k_r$ (this rate is sometimes written $k_{em} = \kappa k_r$ [30; 33]). Comparing the enhancement $\eta_F$ in the saturation regime to the case of weak excitation, it turns out that $\eta_F$ in the weak excitation regime is larger by a factor $(I_e^*/I_e)(\tau^*/\tau)$, which amounts to the gain in the excitation intensity divided by the fluorescence lifetime reduction. Depending on the interplay between excitation enhancement and quenching losses, high fluorescence enhancement values can be preferentially reached by working in the weak excitation regime (most common cases), or at fluorescence saturation (in the case of strong quenching losses). However, it must be kept in mind that the saturation intensity increases when the reduction of the fluorescence lifetime. Therefore reaching the saturation regime will require more excitation power in the case of strong quenching, that may even induce photodamage to the molecule or to the structure.

Figure 2 illustrates the dependence of the fluorescence enhancement factor on the excitation intensity, in the example case of the corrugated aperture displayed in Fig. 1. The fluorescence count rates per molecule in the case of the antenna and the reference solution are presented in Fig. 2(a) versus the excitation power, together with numerical fits according to the general expression Eq. (1) (the CRM for the reference solution has been multiplied by an arbitrary 20x factor to ease viewing). A transition between the regimes of weak excitation and saturation are clearly seen for excitation powers around 1 mW (excitation made through a 0.5 NA objective, so the power to reach saturation are significantly higher as compared to focusing with a high NA objective). The transition towards saturation can be quantified by the saturation intensity $I_s$. For the experiments in Fig. 2(a), we found $I_s^* = 1.2$ mW for the antenna and $I_s = 3.4$ mW for the reference solution [34] (in the case of a 1.2 NA objective, the saturation intensities would be $I_s^* = 130 \mu$W for the antenna and $I_s = 510 \mu$W for the reference solution).

Changing the excitation intensity has a strong influence on the fluorescence enhancement factor, as seen in Fig. 2(b). In the weak excitation regime, the enhancement is maximum ($\sim 80\times$ for this example), while it decreases to $\sim 40\times$ when saturation is reached. This can be directly explained by
the different contributions of the gains in radiative rate, quantum yield, and excitation intensity. $\eta_F$ in the weak excitation regime is larger by a factor $(I_e^*/I_e)(\tau^*/\tau) \approx 2$, which corresponds well to the gain in the excitation intensity ($\approx 5.5$) divided by the fluorescence lifetime reduction ($\approx 2$) as measured separately [33].

2.3 Emitter’s reference quantum yield without the antenna

In this section, we take a closer look at the influence of the emitter’s quantum yield $\phi = k_r/(k_r + k_{nr})$ on the fluorescence enhancement factor. The basic question is how shall we choose $\phi$ for the reference solution (without the antenna) so as to maximize the fluorescence enhancement? Hereafter, the excitation intensity is set to the weak excitation regime $I_e \ll I_s$ (in the saturation regime, the fluorescence enhancement does not depend directly on $\phi$, so the discussion is useless).

With the nanoantenna, the quantum yield is modified to $\phi^* = k_r^*/(k_r^* + k_{nr} + k_{abs}^*)$, where a new non-radiative decay route $k_{abs}^*$ is introduced to take into account the ohmic losses into the metal and non-radiative energy transfers to the free electrons in the metal. It is also assumed that the non-
radiative rate $k_{nr}$ is not affected by the antenna. After some basic algebra, Eq. (4) can be rewritten:

$$\eta_F = \frac{\kappa^* k^*_r}{\kappa k_r} \frac{I^*_e}{I_e} \left( \frac{1}{1 - \phi} + \phi \zeta \right)$$  \hspace{1cm} (7)

with $\zeta = (k^*_r + k^*_{abs})/k_r$. In the limit of a “poor” emitter $\phi \ll 1$, and $\phi \zeta \ll 1$, Eq. (7) resumes to

$$\eta_F = \frac{\kappa^* k^*_r}{\kappa k_r} \frac{I^*_e}{I_e} \quad (\phi \ll 1)$$  \hspace{1cm} (8)

which is the product of the gains in collection efficiency, radiative rate and excitation intensity (this value can also be seen as the enhancement factor found at saturation times the gain in excitation intensity).

In the case of a perfect emitter $\phi \simeq 1$, Eq. (7) resumes to

$$\eta_F = \frac{\kappa^*}{\kappa} \frac{I^*_e}{I_e} \quad (\phi \simeq 1)$$  \hspace{1cm} (9)

if we assume that $k^*_r \gg k^*_{abs}$, meaning that the antenna has a large efficiency. Thus for a perfect emitter, the fluorescence enhancement at weak excitation intensity is given by the product of the gains in collection efficiency and excitation intensity. The fluorescence enhancement in the case of a poor emitter is larger by a factor $k^*_r/k_r$, indicating that in order to maximize the value for $\eta_F$, one should preferentially select emitters with rather low quantum yields (as long as the experimental signal-to-noise ratio is sufficiently high to provide for reliable measurements).

Figure 3 illustrates this discussion, based on the modification of the fluorescence properties calibrated in [33]. $\eta_F$ grows as the reference quantum yield $\phi$ is decreased, up to a plateau for $\phi < 0.02$. Again, the maximum value for the fluorescence enhancement in this example can be significantly different if a perfect dye is used $\eta_F \approx 35$, or if a poor emitter is chosen $\eta_F \approx 150$.

### 2.4 Luminescence collection efficiency

All the formulas presented here for the fluorescence enhancement factor are proportional to the gain in collection efficiency $\kappa^*/\kappa$, independently on the choice for excitation intensity or quantum yield. This is a direct consequence that obviously only the photons that are collected by the setup contribute to the detected fluorescence. Therefore, to maximize the fluorescence enhancement factor, one has to maximize the collection efficiency gain $\kappa^*/\kappa$. This can be done by tuning the antenna so as to maximize the directivity [15] [40] [41], and by minimizing the collection efficiency $\kappa$ used for the reference. In other words, to maximize $\eta_F$, an objective with low numerical aperture should be used in accordance to the peak angular emission of the antenna’s radiation pattern.

Figure 4 displays the influence of the numerical aperture used for fluorescence collection on the detected fluorescence enhancement factor. The antenna used here is again the corrugated aperture presented in Fig. [1]. It was found that the fluorescence radiation pattern with the antenna presented a
Figure 3: Fluorescence enhancement factor versus the dye’s quantum yield $\phi$ in solution (taken without the antenna), in the case of weak excitation. The arrows indicate the two extreme cases of perfect dye ($\phi = 1$) or poor emitter ($\phi \ll 1$). The experimental data is taken from [33].

peak in the direction normal to the sample plane with an angular divergence of $\pm 15^\circ$. Figure 4 presents the computed fluorescence enhancement factor integrated over the whole collection NA. Minimizing the collection NA to values below 0.1 maximizes the fluorescence enhancement factor up to values $\sim 110$, whereas a large collection NA of 1.2 reduces the effective enhancement factor to $\sim 20$ as an effect of angular averaging.

3 Discussion

From the aforementioned investigations on the role of the different experimental parameters on the measured fluorescence enhancement factor, a general “rule of thumb” can be derived: the lower the reference without the antenna, the higher the enhancement factor. In other words, to obtain high enhancement factors, one should preferentially select a weak excitation regime, a dye with low quantum yield and a low collection NA. Of course, this comes at the expense of lower signal (at least for the reference case) and higher noise.

To illustrate the broad range of fluorescence enhancement factors that can be measured using the same nanoantenna design, different computations have been performed using the antenna presented in Fig. 1 with either 0.5 or 1.2 NA microscope objective, 0.01 or 1 quantum efficiencies and in the limits of weak excitation or fluorescence saturation. The results are graphically presented in Fig. 5a). In the extreme case of low reference without the antenna (0.5 NA, $\phi = 0.01$, weak excitation), the fluorescence enhancement is maximum $\sim 150$, while it is minimum $\sim 6$ when the reference is the
highest (1.2 NA, $\phi = 1$, saturation).

This clearly shows that the fluorescence enhancement factor is not an absolute figure of merit for a given nanoantenna. This is in strong opposition with the directivity, which is another figure of merit commonly used to characterize the quality of an antenna design, and which can be intrinsic to the antenna (if properly measured [2, 33, 41]).

The fluorescence enhancement factor is an intuitive metric that is commonly used in surface-enhanced (or metal-enhanced) fluorescence. The experimental setup can be adequately tuned so as to maximize the measured values of $\eta_F$. However, it should be kept in mind that the final goal in the detection of molecules or the generation of single photons is to realize bright sources out of single quantum emitters [12]. Thus the true figure of merit is not the enhancement factor (“how much do we gain”) but instead the fluorescence count rate per emitter (“how much do we have”). High enhancement factors should not be confused with bright sources. To illustrate this, Figure 5(b) displays the detected count rate per molecule corresponding to the cases in (a). To maximize the detection rate, one has to select the conditions of high collection NA, high quantum yield, and high excitation intensity (saturation). These conditions correspond to the ones leading to the minimum fluorescence enhancement factor in Fig. 5(a). Reciprocally, the conditions found for maximum enhancement lead to the minimum detection rates. Taking a low emission for reference and enhancing it (a lot) does not necessarily compensate for the low detection rate to start with. Of course, all this discussion strongly depends on the final application of the nanoantenna–emitter system, and the initial photophysical properties of the emitter.
Figure 5: Fluorescence enhancement factor (a) and fluorescence detection rate per emitter (b) for different numerical apertures (NA) used for collection, different quantum yield \( \phi \) of the emitter in solution (in the absence of the antenna) and in the limit of weak excitation (blue) or fluorescence saturation (red). The antenna used here is the corrugated aperture with five grooves described in Fig. 1 and calibrated in [33].

4 Conclusion

This article has explored the influence of several parameters on the fluorescence enhancement factor with an optical antenna: excitation intensity, emitter’s quantum yield, and collection efficiency. General rules have been derived to obtain high enhancement factors by tuning the experimental conditions without affecting the antenna’s design. Experimental conditions leading to a low reference signal without the antenna should be preferentially selected to maximize \( \eta_F \). This corresponds to weak excitation regime, dye with low quantum yield and low collection NA. General remarks can be drawn from the discussion: (i) the fluorescence enhancement factor is not an absolute figure of merit for a given optical antenna design, (ii) the fluorescence lifetime reduction (Purcell factor) must not be confused with the fluorescence count rate enhancement, and (iii) high enhancement factors do not necessarily indicate bright photon sources.

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