Close Stellar Flybys Common in Low-mass Clusters

Susanne Pfalzner$^{1,2}$ and Amith Govind$^{1,2}$

$^1$Jülich Supercomputing Center, Forschungszentrum Jülich, D-52428 Jülich, Germany; s.pfalzner@fz-juelich
$^2$Max-Planck-Institut für Radioastronomie, Auf dem Hügel 69, D-53121 Bonn, Germany

Received 2021 June 14; revised 2021 July 29; accepted 2021 July 30; published 2021 November 3

Abstract

Numerous protoplanetary disks show distinct spiral arms features. While possibly caused by a range of processes, detailed pattern analysis points at close stellar flybys as cause for some of them. Surprisingly, these disks reside in young low-mass clusters, where close stellar flybys are expected to be rare. This fact motivated us to take a fresh look at the frequency of close flybys in low-mass clusters. In the solar neighborhood, low-mass clusters have smaller half-mass radii than their more massive counterparts. We show that this observational fact results in the mean and central stellar density of low-mass clusters being approximately the same as in high-mass clusters, which is rarely reflected in theoretical studies. We perform $N$-body simulations of the stellar dynamics in young clusters obeying the observed mass–radius relation. Taking the mean disk truncation radius as a proxy for the degree of influence of the environment, we find that the influence of the environment on disks is more or less the same in low- and high-mass clusters. Even the fraction of small disks ($<10$ au) is nearly identical. Our main conclusion is that the frequency of close flybys seems to have been severely underestimated for low-mass clusters. A testable prediction of this hypothesis is that low-mass clusters should contain 10%–15% of disks smaller than 30 au truncated by flybys. These truncated disks should be distinguishable from primordially small disks by their steep outer edge.

Unified Astronomy Thesaurus concepts: Young star clusters (1833); Circumstellar disks (235)

1. Introduction

The observed diversity in the structure of protoplanetary disks (e.g., Andrews 2020; van der Marel et al. 2021) and the planetary systems (e.g., Kaltenegger 2017; Miguel et al. 2020, and references therein) triggers a renewed interest in the question of the effect of the environment on planet formation (recent examples being Cai et al. 2018; Winter et al. 2020; Adibekyan et al. 2021; Dai et al. 2021). One way that the environment influences a forming planetary system is close stellar flybys. These stellar flybys can potentially truncate or even completely destroy the protoplanetary disks, thus influencing the total size and frequency of planetary systems (e.g., Scally & Clarke 2001; Adams et al. 2006; Olczak et al. 2006; Rosotti et al. 2014; Steinhauser & Pfalzner 2014; Portegies Zwart 2016; Vinecke & Pfalzner 2016; Concha-Ramírez et al. 2019; Jiménez-Torres 2020; Concha-Ramírez et al. 2021). Close stellar flybys are expected to be most common in the central areas of high-mass clusters but rare in low-mass associations. Finding signs of the stellar flybys seemed for a long time elusive, as only a handful of objects showed the characteristic spiral arm patterns. The situation changed when the Atacama Large Millimeter/submillimeter Array (ALMA) telescope allowed for the first time the production of highly resolved imaging of protoplanetary disks. Suddenly, characteristic spiral structures are abundantly observed (Meru et al. 2017; Dong et al. 2018; Long et al. 2018; Andrews et al. 2018a). Spiral structures can be induced by either a companion or a stellar flyby, so that undetected companions can be the reason behind the pattern. However, the repeated interaction with a bound companion generates more compact spirals.

Close stellar flybys are expected to be most common in locations of high stellar density. However, the disks with spiral arm patterns are often located in low-mass young associations. In several cases, the spiral pattern details clearly point to a flyby rather than a companion. So ongoing (or past) flybys have been suspected for RW Aur (Cabrit et al. 2006; Dai et al. 2015; Rodríguez et al. 2018), AS 205 (Kurtovic et al. 2018), HV Tau and Do Tau (Winter et al. 2018), FU Ori (Beck & Aspin 2012; Takami et al. 2018; Pérez et al. 2020), V2775 Ori (Zurlo et al. 2017), V1647 Ori (Principe et al. 2018), Z CMa (Takami et al. 2018), SU Aur (Akiyama et al. 2019), and UX Tau (Ménard et al. 2020). These systems often show other signs typical for a close stellar flyby, such as disk truncation and warping accompanied by dimming and outburst events (Cuello et al. 2019). Assuming that close stellar flybys indeed induced the spiral pattern, it would mean that close flybys in low-mass associations are more common than generally believed. Here we test this hypothesis by performing cluster simulations based on the observed properties of young (<3 Myr) stellar groups typical for the solar neighborhood.

First, we motivate why close encounters might be more common than expected in low-mass clusters (Section 2). The central argument here is that low-mass clusters have a smaller size than high-mass clusters, leading to a higher mean stellar density. In Section 3 we describe the method we use to simulate the flyby dynamics in clusters and justify the approximations made in our toy model. The main result of our simulations is that close flybys are actually so common in low-mass clusters that their effect on disks might be comparable to that in high-mass stellar groups. We show that our results agree with observational results of the frequency of small disks in low-mass clusters. Finally, we make two predictions based on our simulation results that dedicated observations could test. These predictions link to the interpretation of disk and planetary system diversity.
2. Low- versus High-mass Stellar Groups

In the context of observations, it is often stated that a sizable effect by the environment on the disks happens only in areas with local stellar number density exceeding $n = 10^4 \text{ pc}^{-3}$ (Gutermuth et al. 2005). Only here are close stellar flybys expected to happen at a sufficiently high frequency. It is a standard argument that such high stellar densities are exclusively found in the dense central areas of high-mass clusters containing several thousand stars (Adams 2010; Malmberg et al. 2011; Dukes & Krumholz 2012; Craig & Krumholz 2013; Parker 2020; Winter et al. 2020). The central area of the Orion Nebula Cluster (ONC) is often referred to as the prime example of such a close-by dense environment. Figure 1(a) seems to confirm the expectation that only clusters with a high number of stars, and therefore mass, exceed the above-noted stellar density limit. It shows the stellar density distribution for stellar groups with different numbers of stars assuming a King profile with a half-mass radius of $R_{\text{hm}} = 1.3$ pc. Only the stellar groups with $\geqslant 4000$ stars reach central densities exceeding the threshold of $10^4 \text{ pc}^{-3}$. Based on this expectation, so far, the effect of flybys was preferentially simulated for relatively high mass clusters containing $N \geqslant 1000$ stars, where $N$ denotes the number of cluster members (e.g., Scally & Clarke 2001; Olczak et al. 2010; Vincke et al. 2015; Vincke & Pfalzner 2016; Parker 2020; Concha-Ramírez et al. 2021).

However, there is a potential problem with the above argument. Only if one considers low- and high-mass stellar groups of the same size does a high-mass group always have a higher central density than a low-mass group. However, if one looks at the properties of young stellar groups in the solar neighborhood, the equal-size assumption is not applicable. The nearby young stellar groups ($< 2 \text{ kpc}, \text{ age } < 10 \text{ Myr}$) show a general trend that low-mass stellar groups have a smaller size than high-mass ones. This is illustrated in Figure 2(a) for the data given in Lada & Lada (2003) and in Figure 2(b) for the recent cluster sample from Kuhn et al. (2019). More examples can be found in Pfalzner et al. (2016). The relation between a cluster’s mass and its half-mass radius can be approximated by

$$M_c = C R_c^\gamma,$$  

(1)

where $M_c$ denotes the cluster mass, $C$ is a constant, $R_c$ is the cluster half-mass radius, and $\gamma$ is the scaling exponent. The constant $C$ and the scaling exponent $\gamma$ typically differ somewhat between considered observational data owing to observational uncertainties in the cluster masses and radii. Note, in particular, that the cluster size values for the same cluster can differ considerably between different samples. The reason is methodological differences, for example, in cluster member identification, size definitions, and data being taken at different wavelengths (for a more detailed discussion on the reasons for individual differences see Pfalzner et al. 2016). It is essential that here standardized methods are developed soon. However, for all investigated data compilations, the scaling exponent lies typically in the range $1.6 - 2.1$ (Pfalzner et al. 2016). Using the full data set by Kuhn et al. (2019), we obtain a best fit for $C = 1263$ and $\gamma = 2.09$. Relation (1) holds only for the relatively short-lived stellar groups in the solar neighborhood. It does not apply to the more compact young clusters that develop into long-lived clusters located at larger distances in the Galaxy’s spiral arms (see Pfalzner & Kaczmarek 2013). The data set by Kuhn et al. (2019) contains two clusters that likely develop into long-lived clusters—the distinctly more compact clusters Tr 14 and M17, which also are of much higher mass than the rest of the sample. If we exclude these two clusters, the

---

3 In the following we use the term high-mass and high-N clusters as synonyms.
best-fit parameters change to $C = 1032$ and $\gamma = 1.9$. However, whichever homogeneous sample of young stellar groups in the solar neighborhood one uses, the general trend of an increase in half-mass radius with cluster mass always persists.

Thus far, this trend of smaller sizes for low-mass clusters has been largely neglected in simulations that concentrate on the effect of stellar flybys. An exception are the works by Adams et al. (2006), who derived an equivalent relation but expressed in terms of the number of stars in the cluster, $N$. They also applied their $N/R_c$ relation to their cluster simulations (Adams 2010; Adams et al. 2014) but mainly concentrated on the effects of external photoevaporation and supernova enrichment, while Proszkow & Adams (2009) looked at the flyby history in different types of clusters, including that of low-mass clusters, but did not consider the consequences of close flybys in such environments in detail. Supernova explosions and external photoevaporation require the presence of massive stars to be efficient; therefore, low-mass clusters are basically unaffected by these two environmental processes. We will see in the following that the situation is completely different for the process of close stellar flybys.

Apart from these works, it was mostly assumed that cluster mass and size are uncorrelated. Therefore, either a parameter grid of sizes and masses was investigated without connecting to the mass–size relation in young clusters, or it was assumed that all clusters have approximately the same size when fully formed. The latter approach seemed reasonable, as theoretical models that backward-engineered the initial sizes of clusters (Marks & Kroupa 2012) indicated that the considered clusters all developed from an initial size of $\sim 0.1$ pc independent of their mass. However, the considered clusters spanned over an age range of several hundred Myr and therefore contained a large fraction of long-lived open clusters. As Figures 2(a) and (b) demonstrate, this conclusion is not necessarily transferable to the short-lived ($<10$ Myr) stellar groups in the solar neighborhood.

Applying the relation $\rho = 3M_c/4\pi R_c^3$ to mass and radius values from Figures 2(a) and (b), the resulting mean density in the respective stellar is shown in Figure 2(c). It can be seen that the mean density in low-mass stellar groups is not only not lower but indeed higher than in high-mass clusters. However, the question is whether these average densities matter here. They are all well below the threshold density of $n = 10^4$ pc$^{-3}$ for a sizable effect on the disks. Therefore, we look in Figure 1(b) at the stellar mass distributions again, but this time with the half-mass radius chosen according to the observed relation given by Equation (1). It can be seen that for these observationally motivated cluster sizes, independent of their mass, all clusters have areas where the central density exceeds the threshold density of $n = 10^4$ pc$^{-3}$. Actually, in low-mass clusters, the relative area above this threshold is higher than in clusters of higher mass. Given the relatively small number of stars in low-mass clusters, the actual number of stars in this area is also small. However, the fraction of stars in the high-density area is higher in low-mass clusters than in high-mass clusters.

Besides, using the number density as a measure for a potential effect of the environment has its limitations, and its physical meaning is questionable, especially for low-mass clusters. What really matters is the probability for close interactions or the mean distance traveled to have such an
interaction. A star will have to have crossed the cluster several times in low-mass clusters before it has such close interaction. Nevertheless, motivated by the above estimates of the theoretical central stellar densities in the observed low-mass clusters, we performed detailed simulations of the encounter dynamics in such environments to obtain a better understanding of the flyby dynamics in low-mass clusters. In the following section, we describe the numerical method, including the approximations made in this approach.

3. Numerical Method

3.1. Cluster Simulations

Our simulations start during the embedded phase assuming that star formation is completed. After a time \( t_{\text{emb}} \), gas expulsion is taking place, resulting in cluster expansion. Also, a standard method in cluster dynamics simulations (e.g., Lada et al. 1984; Scally & Clarke 2001; Banerjee & Kroupa 2017), it is in some sense a toy model, as it avoids the complexity and numerical challenges the formation of massive clusters still faces. Thus, the simulation sets in only when all stars are formed, and we take the mass–radius relations discussed in Section 2 at face value. Naturally, any high-mass cluster must go through a phase where it starts initially with a small number of stars and gradually grows to its final size. However, such cluster formation simulations are still limited to clusters containing \( \lesssim 1000 \) stars, at least for the resolution required here. Therefore, we revert to the often-used method of following the stellar dynamics in the fully formed clusters instead. The limitations of this approach are discussed in Section 5.

We perform simulations of the dynamics of clusters containing \( N \) stars using the simulation code Nbody6+++. In the simulations, a star is represented by a test particle with a given mass, position, and velocity. The particles’ positions are chosen so that the resulting stellar number density distribution obeys a King profile (King 1966). The reason is that King profiles seem to present young clusters well (Hillenbrand & Hartmann 1998; Nürnberg & Petr-Gotzens 2002; Harfst et al. 2010); however, there is no general observational agreement whether \( W = 7 \), \( W = 8 \), or \( W = 9 \) is the best choice. Here we mostly use a King profile with \( W_0 > 9 \), but we also discuss in Section 5 the role of the chosen profile for our results.

The individual test particles are assigned masses following the initial mass function (IMF) by Kroupa (2001),

\[
\xi(m) \propto \begin{cases} 
  m^{-0.3} & 0.01 \leq m M_\odot^{-1} < 0.08 \\
  m^{-1.3} & 0.08 \leq m M_\odot^{-1} < 0.5 \\
  m^{-2.3} & 0.5 \leq m M_\odot^{-1} 
\end{cases}
\]  

with the lower mass limit set to 0.08 \( M_\odot \) (hydrogen burning limit) and an upper mass limit of 150 \( M_\odot \), which is the accepted upper mass limit (Figer 2005; Weidner & Kroupa 2006).

Initially, all cluster stars are single stars, meaning primordial binaries as excluded. This approximation is chosen for simplicity in the consecutive processing of the effect of flybys on disk size, where the inclusion of primordial binaries would significantly increase the complexity. The absence of primordial binaries might lead to underestimated ejections from the cluster owing to strong few-body interactions (Heggie 1975; Hills 1975). For a more detailed discussion of omitting binaries in this type of study, see Olczak et al. (2006). Besides, binaries can accelerate a cluster’s expansion process and reduce the encounter rate faster (Kroupa 2001; Kaczmarek et al. 2011).

Potentially existing initial mass segregation in the clusters was neglected. The occurrence of mass segregation within clusters is still under debate, whether it is primordial—found in the dense core phase of the cluster formation process (Dib et al. 2010; Dib & Henning 2019)—or it is a result of the early dynamical evolution of the cluster (Pelupessy & Portegies Zwart 2012; Domínguez et al. 2017).

The cluster members are given a velocity following a Maxwellian distribution involving the random sampling of Gaussian deviates for the individual velocity components. We assumed that the cluster is in virial equilibrium. During the embedded phase, the gas cloud is implemented as a background potential. The effect of gas expulsion is modeled as instantaneous, as the timescale for gas expulsion is sufficiently short (Geyer & Burkert 2001; Melioli et al. 2006; Portegies Zwart et al. 2010). The gas removal leaves the cluster in a supervirial state, and as a result, the cluster expands to return to a new virial equilibrium state. Stellar evolution has not been included in this work, as it has limited influence on the results, especially on the low-mass clusters that we focus on here.

We performed three sets of simulations differing in the choice of the cluster size. For sets 1 and 3 the cluster half-mass radius was chosen according to Equation (1), whereas for set 2 the cluster size was a fixed value of 1.3 pc. For set 1 \( C \) and \( \gamma \) were chosen according to Pfalzner et al. (2016), and for set 3 we used the values derived in Section 2 based on the data by Kuhn et al. (2019). For each of these sets, we performed simulations for clusters with \( N = 200, 1000, 4000, \) and 10,000 test particles. For set 2 we modeled also clusters with \( N = 16,000 \) to be able to compare to the results of Pfalzner et al. (2016) for high-mass clusters. The simulation parameters are summarized in Table 1. It also provides the timescales relevant to cluster dynamics, namely, the crossing time, \( t_{\text{cross}} \), and the two-body relaxation time, \( t_{\text{rel}} \). Statistical significance of the results has been ensured by always performing many simulations (\( N_{\text{sim}} \)) with different seeds for the spatial distribution. This number of runs was chosen so that \( N_{\text{stars}} \times N_{\text{sim}} \approx 5 \times 10^5 \), which is necessary to obtain statistically significant results. More detailed information on the cluster dynamics method and its limitations is given in Vincke & Pfalzner (2016).

Ideally, one would simulate the disk evolution around each star within the cluster evolution simulation to determine the effect of the cluster environment on the disks. However, currently such simulations are computationally too expensive to be performed for clusters with large \( N \), unless one restricts them to a single simulation, simulation periods of \( < 1 \) Myr, and/or single-mass representation (Rosotti et al. 2014). The latter approach does not allow the comparative statistically significant study we envisage here. Therefore, we apply a two-step approach, where the first step consists of the above-described cluster simulations. While running these simulations, the encounter history for each star is recorded, meaning that for each star the mass ratio and periastron distance of each close flyby is listed. In the second step, the truncation disk size for each of the close-flyby events is calculated. Afterward, we use the mean value of the final truncation disk size to measure the cluster environment’s effect on forming planetary systems.
Table 1

Initial Cluster Parameters for the Simulation Campaign Using Mass–Radius Dependencies

| Model  | $N$ | $N_{\text{sim}}$ | $M_\text{c}$ (M$_\odot$) | $R_{\text{sim}}$ (pc) | $M_\text{i}$ (M$_\odot$) | $t_{\text{emb}}$ (Myr) | $t_{\text{cross}}$ (Myr) | $t_{\text{relax}}$ (Myr) |
|--------|-----|------------------|--------------------------|------------------------|-------------------------|------------------------|--------------------------|------------------------|
| Set 1  | $\gamma = 1.7$ | | | | | | | |
| P200   | 200 | 1685             | 117.99                   | 0.26                   | 393.31                  | 2.0                    | 0.10                     | 2.10                   |
| P1000  | 1000| 604              | 589.97                   | 0.67                   | 1966.57                 | 2.0                    | 0.18                     | 14.20                  |
| P4000  | 4000| 147              | 2359.88                  | 1.51                   | 7866.27                 | 2.0                    | 0.31                     | 78.36                  |
| P10000 | 10,000| 95             | 5899.71                  | 2.59                   | 19,665.68               | 2.0                    | 0.44                     | 247.35                 |
| Set 2  | $\gamma = 2.0$ | | | | | | | |
| K200   | 200 | 1484             | 117.99                   | 0.32                   | 393.31                  | 2.0                    | 0.14                     | 2.90                   |
| K1000  | 1000| 492              | 589.97                   | 0.70                   | 1966.57                 | 2.0                    | 0.19                     | 15.01                  |
| K4000  | 4000| 110              | 2359.88                  | 1.35                   | 7866.27                 | 2.0                    | 0.26                     | 65.87                  |
| K10000 | 10,000| 71             | 5899.71                  | 2.09                   | 19,665.68               | 2.0                    | 0.32                     | 178.68                 |
| Set 3  | $R_c = 1.3$ pc | | | | | | | |
| V200   | 200 | 864              | 117.99                   | 1.3                    | 393.31                  | 2.0                    | 1.11                     | 23.48                  |
| V1000  | 1000| 167              | 589.97                   | 1.3                    | 1966.57                 | 2.0                    | 0.50                     | 38.40                  |
| V4000  | 4000| 61               | 2359.88                  | 1.3                    | 7866.27                 | 2.0                    | 0.25                     | 62.37                  |
| V10000 | 10,000| 12             | 9439.53                  | 1.3                    | 31,465.09               | 2.0                    | 0.12                     | 105.00                 |

Note.—Here $N$ denotes the number of cluster members, $N_{\text{sim}}$ the number of simulations for each cluster model, $t_{\text{emb}}$ the duration of the embedded phase, $M_\text{c}$ the stellar mass of the cluster, $R_{\text{sim}}$ the half-mass radius, $M_\text{i}$ the total cluster mass (stars + gas), $t_{\text{cross}}$ the cluster crossing time, and $t_{\text{relax}}$ the relaxation time. Set 1 is based on the relation found in Pfalzner et al. (2016), set 2 for the relation derived in Section 2 for the data by Kuhn et al. (2019), and set 3 for a constant cluster size as modeled in Vincke & Pfalzner (2016).

3.2. Disk Truncation

We start with the artificial situation of all disks having a size of 1000 au initially. This value is typical for the top end of the size of observed disks (Andrews et al. 2018). The reason is that we only intend to obtain a measure of the influence of the environment rather than a realistic representation of the disk sizes in a specific cluster. Thus, we obtain the size that a standard disk is truncated to owing to the close flybys of a particular cluster environment. This truncation disk size is obtained in the following way:

In this work, all encounters were assumed to be parabolic, prograde, and coplanar, using the results of a parameter study of star–disk encounters performed by Breslau et al. (2014). In this case, the truncation disk size $r_{\text{disk}}$ after the flyby can be approximated as

$$r_{\text{disk}} = \begin{cases} 0.28 \cdot r_{\text{peri}} \cdot M_2^{0.32}, & \text{if } r_{\text{disk}} < r_{\text{previous}} \\ r_{\text{previous}}, & \text{if } r_{\text{disk}} \geq r_{\text{previous}} \end{cases}$$

where $r_{\text{peri}}$ is the periastron distance between the two stars involved in a close flyby in au. $M_2 = M_2/M_1$ is the mass ratio of the two stars, with $M_1$ being the mass of the disk-hosting star and $M_2$ that of the perturber star. $r_{\text{previous}}$ is the disk size before the encounter.

Inclined or retrograde flybys are less efficient to remove material from the disk, and the disk truncation radii are therefore larger (Clarke & Pringle 1993; Bhandare et al. 2016). However, the difference to coplanar flybys is not extremely large. Applying the result for coplanar flybys means that the truncation radii have to be regarded as lower limits. Similar, hyperbolic flybys are less effective in disk truncation than parabolic ones. However, more eccentric encounters are significantly more common in higher-mass clusters. Since our study focuses on low-mass clusters, approximating the flyby path as parabolic is likely justified. Moreover, we apply these simplifications in all simulations identically, so the relative differences between the diverse cluster environments should not be affected. Here, only a summary of the method has been provided; we refer the reader to Breslau et al. (2014) for more information on the disk size determination during close stellar encounters.

3.3. Observational Uncertainties

As mentioned in Section 1, the exponent in the derived mass–radius relations for young stellar clusters in the solar neighborhood varies between $\gamma = 1.7$ and 2.0, and that of the constant spans the range of $C = 359-1263$. These variations are caused by the differences in the sample of clusters considered, the observation being at different wavelengths, and different cluster mass and size definitions. In some studies, the cluster size is defined as the maximum extent of the cluster; in others, the half-mass or half-light radius. Similarly, the definition of cluster mass varies from study to study. Some studies give the number of observed stars, while some correct for the IMF. Therefore, one finds sometimes, even for the same clusters, differences of up to a factor 2. A detailed discussion of the involved difficulties can be found in Pfalzner et al. (2016).

As Figure 1(c) shows, these differences in mass and radius translate into equivalent differences in stellar density. Therefore, one could worry whether the specific mass–radius relations studied here are of any relevance. In this study, we included two extreme cases in the sense that they cover the broad range of possible values for the mass–radius relation. Set 1 of our simulations (P200–P10000) stands for the strongest dependence on the cluster mass, whereas set 2 covers the weakest case. In the following, we show the results from both sets 1 and 2 and contrast them to those of set 3, standing for a constant cluster size to illustrate the extent to which previous simulations might have underestimated the effect of close stellar flybys in low-mass clusters.
The mass–radius relation is only well constrained for clusters with $N \gtrsim 2000$ stars, as there are many clusters in the solar neighborhood in this membership range. Clusters containing $N \lesssim 2000$ are rare in the solar neighborhood. There are only a handful of such member-rich young clusters. Therefore, the mass–radius relationship is probably only applicable to clusters with $N < 5000$ stars. We discuss this issue in more detail in Section 6.

4. Simulation Results

In Section 2 we demonstrated that for the clusters in the solar neighborhood initial conditions obeying a mass–radius relation (Equation (1)) are more realistic than those assuming a constant radius. Here we will investigate the consequences for the interaction dynamics in low-mass clusters. First, we study the development of the mean stellar density with time for low-mass clusters. The mean stellar density corresponds to the mass-contained density in the volume defined by the cluster half-mass radius (equivalent to the 50% Lagrangian radius). Figure 3 shows that all low-mass clusters ($N \lesssim 1000$) follow the same overall evolutionary pattern. During the initial embedded phase, the stellar density remains almost constant. However, when the gas is expelled, the clusters expand, which means a significant decrease in the mean stellar density. The cluster settles eventually in a new
The Astrophysical Journal, 921:90 (13pp), 2021 November 1

The difference in the encounter history of clusters obeying the mass–radius relation lies on the quantitative level (see Figure 3(a)). Whereas for the standard model V200 the mean stellar density is about 10 $M_\odot$ pc$^{-3}$ during the 2 Myr of the embedded phase, for K200 and P200 it is $\approx 1000$ $M_\odot$ pc$^{-3}$, therefore about a factor of 100 higher for models P200 and K200. All clusters decline to approximately the same mean density of $\approx 0.5$–1.0 $M_\odot$ pc$^{-3}$, after gas expulsion. However, the standard model only decreases to 1/10 of its initial value, whereas models P200 and K200 experience a much more drastic decrease to a factor of $\approx 1000$ lower mean stellar density. Besides, P200 and K200 have already reached their new (semi)equilibrium state after 6 and 8 Myr, respectively, whereas V200 keeps steadily declining, as it has not reached its new equilibrium at the end of the simulation at 10 Myr and will probably require 20–40 Myr to reach this state.

Figure 3(b) shows the same situation of clusters containing 1000 stars, where the difference between the various models is much less pronounced. In the embedded phase, model V1000 shows only a factor 7–10 lower mean stellar density than the other two sets. The mean stellar density in models P1000 and V1000 is nearly indistinguishable over the entire period of 10 Myr. Our simulations of high-mass clusters $N = 4000$ show that the differences in stellar density vanish completely. In summary, for clusters with $N < 1000$, taking the mass–radius relation matters most.

Naturally, the encounter history directly reflects the development of the stellar density (see Figures 3(c) and (d)). Here we defined encounters as those stellar flybys that have the potential to reduce the disk size to less than 100 au using the equation given in Breslau et al. (2014) (Equation 3). The first few time steps are to some degree affected by the random setup. This leads to some artificial close encounters during the first few time steps, which becomes obvious in the low-number statistics of V200. Afterward, the encounter frequency is about a factor 20–25 higher for models P200 and K200 than for the standard model V200 during the embedded phase (see Figure 3(b)). The difference reduces to a factor of a few after ages $> 4$ Myr.

Next, we want to define a measure for the effect of stellar flybys on disks and forming planetary systems. Here we use the mean truncation disk size, which we obtain by initially attributing a 1000 au sized disk to each star. Using the recorded flyby history, we determine the truncation of the disk using Equation (3) for each star due to all flybys that it encounters over 10 Myr. This truncation disk radius should not be confused with observed disk sizes, as most stars will have significantly smaller initial disk sizes than 1000 au. At this point, it is just a measure that allows the comparison of the strengths of the environmental effect in different cluster environments. The relation to observed disk sizes is discussed in Section 5.

From the just-discussed encounter history, it seems already obvious that the diverse low-mass cluster models should lead to different truncation disk sizes. Figure 4 shows the mean disk size within clusters at an age of 10 Myr as a function of number of cluster members for all cluster models listed in Table 1. To start with, we only consider clusters containing between 200 and 4000 stars. The reason is that the mass–radius relation is only observationally constrained for this mass range and probably not applicable for clusters containing several tens of thousands of stars. For the low-mass clusters ($N = 200$), the mean truncation disk size is $\approx 900$ au for the standard model (V200). Only a few stars actually experience close flybys. By contrast, the observationally motivated models lead to much lower mean truncation radii ($\approx 481$ au for model P200 and $\approx 551$ au for model K200). This shows that the effect of the environment in real embedded clusters is much stronger than mostly anticipated so far. Our results translate to a mean close-flyby distance of 1000–1500 au in low-mass clusters. This agrees with the results of $\approx 1000$ au by Proszkow & Adams (2009) for their low-mass clusters ($N = 300$).

However, Figure 4 contains an additional important piece of information, namely, that the overall effect of stellar flybys should be approximately the same for clusters that contain 200 stars as those containing 4000 stars. The latter is representative for clusters similar to the ONC. For model set 2 we obtain a mean disk truncation radius of $\approx 551$ au for $N = 200$ (K200) and $\approx 607$ au for $N = 4000$ (K4000). For model set 1, the lower truncation radius for low-mass relative to high-mass clusters would even indicate a stronger flyby dynamics in low-mass clusters. This is in stark contrast to the standard model, where the mean truncation disk size for low-mass clusters is relatively large with $\tau_T(V200) \approx 918$ au, compared to $\tau_T(V10000) \approx 403$ au for the high-mass clusters, which reproduces the results presented in Vincke & Pfalzner (2016). Their main finding was that given the same initial cluster radius, the median truncation disk size decreased for an increasing number of cluster members.

As discussed in Section 3.3, the mass–radius relation probably does not hold for clusters with more than 5000
members. Therefore, the disk truncation radii are shown in a lighter color in Figure 4. We expect that for \( N = 10,000 \) the standard model is a better approximation of reality. Here the disk truncation radius is slightly smaller (420 au) than for the low-mass clusters, and the effect of the flybys is a bit stronger than in low-\( N \) clusters. Nevertheless, the difference in the effect of flybys in low-\( N \) and high-\( N \) clusters is much less pronounced than previously anticipated.

However, the mean truncation disk size gives only limited information about the interaction dynamics in clusters. The distribution of truncation disk sizes gives some valuable additional insights. The left panel of Figure 5 shows the distribution of truncation disk sizes for low-mass clusters (\( N = 200 \)); the right panel, that for high-mass clusters \( N = 10,000 \). In both panels, the results for an initial constant cluster size of 1.3 pc (orange bars) are compared to those obeying the mass–radius relation (blue bars). The distribution is shown over the entire size range from 0 to 1000 au (bottom panels), but also a zoom-in for disk sizes <100 au is given with bin sizes of 10 au (top panel). Looking at the bottom panel, one sees that the truncation disk size distributions for models P200 and V200 differ considerably. In the standard model V200 (orange bars), approximately 95% of all disks have a disk size close to the initial disk size of 1000 au. Those are virtually unaffected by close flybys. In model P200, the situation is very different, with nearly 87% of disks having disk sizes much smaller than 1000 au at the end of the simulation. This high percentage for model P200 means that most disks are affected by close flybys, with close to 30% being reduced to sizes smaller than 100 au. Zooming in on the disks with sizes less than 100 in the top panel of Figure 5, astonishingly, in model P200, approximately 5% of disks are even truncated to sizes of less than 10 au. This result strongly indicates that the frequency of close stellar flybys has been severely underestimated for low-mass clusters.

The truncation disk size distribution in model P200 (blue bars in the left panel) is surprisingly similar to that of model V10000, the standard model for high-\( N \) clusters (orange bars in the right panel). In P200, 80% of disks are significantly affected by close flybys. Approximately 27% of disks are even reduced to less than 100 au, and approximately 4.5% of disks truncated to less than 10 au. The results are very similar for the steeper mass–radius relation derived from the Kuhn data (as shown in Figure A1). Considering these fractions of truncated disks demands a fundamental change of our view of the role of the environment in low-mass clusters, namely, the effect of the environment by close stellar flybys is approximately the same in high- and low-mass short-lived clusters.

Our results demand a considerable change in how we think about the influence of the environment in low-mass clusters. Therefore, we want to make sure that the result holds against closer scrutiny. Therefore, we performed some additional tests to exclude that particular choices in our simulations lead to an overabundance of close flybys in low-mass clusters.

In Section 3 we chose a King \( W = 9 \) profile for the stellar distribution, as this profile corresponds to the observed density profile of the ONC (Hillenbrand & Hartmann 1998). However, low-mass clusters contain fewer stars, so that profile fitting is less well constrained than for high-mass clusters. Therefore, it is unclear whether a King (\( W = 7 \)) profile and the even much flatter Plummer profile are equally good or even better choices for low-mass clusters. Figure 6(a) shows a comparison of different King profiles (\( W = 6, 7, 8, \) and 9) and a Plummer profile for a cluster of mass 5000 \( M_\odot \) and a half-mass radius of 1.3 pc. The central stellar density is highest for a King profile \( W = 9 \) and lowest for a Plummer profile; this leads to more close flybys than in clusters with a Plummer profile. Therefore, there exists the potential risk that the choice of profile could give unrealistically high rates of close encounters in low-mass clusters. We tested whether the choice of the stellar density profile is responsible for the high
frequency of close flybys in low-mass clusters by also performing simulations with a Plummer profile for the entire set of cluster parameters. Figure 6(b) shows a comparison of the mean truncation disk size shown in Figure 4 obtained by using a King profile with those applying a Plummer profile. It can be seen that, for high-mass clusters ($N = 10,000$) in King-type clusters, disks are on average truncated to smaller sizes than in Plummer-type clusters. This result confirms the expectation. However, there is virtually no difference between the mean truncation radius for the two types of profiles for low-mass clusters. The reason is that in high-mass clusters a considerable number of stars actually stay for a relatively long time in the central high density. In contrast, in low-mass clusters the stars quickly pass through this area. In conclusion, our result for the low-mass clusters still holds if we apply a Plummer distribution instead of a King profile.

As shown in Table 1, we simulated 1685 different realizations of model P200. The stellar masses are randomly chosen according to the IMF; therefore, some low-mass clusters contain high-mass stars. Such high-mass stars inevitably lead to gravitational focusing, which can cause rapid disk destruction. Next, we test whether the result could be biased by gravitational focusing in those low-mass clusters containing high-mass stars. Therefore, we divided our complete set of simulations into two subsets. One consisted of all those clusters that contained one or more high-mass stars ($M > 20 M_\odot$), and the other subset was devoid of high-mass stars. We obtained approximately the same values for the disk truncation radius for both subsets and the entire ensemble. We conclude that clusters containing high-mass stars do not influence the result in any way.

5. Consequences and Observational Tests

From our simulations, it follows that in low-mass clusters the effect of the environment on disks is comparable to that in high-mass clusters. The question is how one can test this hypothesis. In the following, we point out possibilities of how high-resolution observations of disks in low-mass clusters and statistics of exoplanet orbital properties could be utilized to test this hypothesis.

5.1. Disk Sizes and Outer Edge Geometry

We pointed out in Section 2 that we start our simulations with all stars being initially surrounded by a 1000 au sized disk. Therefore, the resulting disk sizes are referred to as truncation disk sizes, as they are primarily a measure of the interaction dynamics. In reality, clusters will likely form with a broad spectrum of disk sizes; however, the primordial disk size distribution is difficult to access, as it is determined in the observationally difficult-to-access deeply embedded phase. Most likely, most disks will be considerably smaller than the 1000 au used here. However, a comparison with observations might be feasible nevertheless for those disks that are truncated to sizes considerably smaller than 100 au. For them, the connection to the initial assumed disk size is erased by the close flyby. In the following, we will compare the relative number of disks smaller than 100 au in our simulation to those in observations being fully aware of the limitations of this approach.

This work focuses on young low-mass clusters in the solar neighborhood. An ideal example cluster to test our results would be IC 348 or LkHα 101. Unfortunately, for both clusters, no information about their disk size distribution exists so far. More information on disk sizes in the literature can be found for low-mass star-forming regions like Taurus-Auriga, Ophiuchus, and Lupus. These regions do show clustering of stars; however, whether these stellar groups are actually bound and dynamically act as a cluster is uncertain. Luhman (2018) found a total of 427 candidate members of the Taurus region, which he divided into four groups with around 50–150 stars. Despite not being the ideal candidate, we concentrate our comparison on the Taurus region because five out of the eight members...
The disk sizes for RW Aur A and B were taken from Rodriguez et al. The red symbols indicate the location of the stars for which Andrews et al. determined disk sizes. Disks with sizes smaller than 30 au are indicated as red crosses, whereas disks with sizes exceeding 30 au are shown as circles. The disk sizes for RW Aur A and B were taken from Rodriguez et al. (2018).

Examples where stellar flybys are suspected as the reason for the spiral arm structures are located in the Taurus region. Figure 7 shows the location of these systems (blue circles) in the Taurus region. While some systems in isolation exist, the majority reside in regions of relatively high stellar density.

In the previous sections, we concentrated on modeling disk sizes. During the past few years, high-resolution observations of protoplanetary disks found that disk sizes span over a wide range and that gas and dust disk sizes can differ considerably, with gas disk sizes usually being considerably larger than the dust disk sizes. Tripathi et al. (2017) find in their high-resolution (sub)millimeter survey of dust continuum emission in Taurus and Ophiuchus that in the 50 studied protoplanetary disks the most common disk sizes are larger than 100 au, but with some disks being considerably smaller. Andrews et al. (2018b) extended this study to include 56 disks in the Lupus star formation rate, finding a similar range in disk size to that on Taurus but with relatively more small disks (<30 au). Najita & Bergin (2018) find that in the Taurus region many disks are larger than 200 au, but there is a large spread in the sizes of Class II gas disks at any age, including a population of tiny Class II gas disks. They suggest that the small sizes may result from processes such as photoevaporation, disk winds, or truncation by orbiting low-mass companions.

The results presented here show that stellar interactions have the potential to produce such small disks even in low-mass clusters. For our model P200, representative for low-mass clusters, we find that while most disks are larger than 100 au, approximately 10%–30% of disks are considerably smaller than 100 au. This compares well with the observed fraction of small-sized disks in low-mass star-forming regions. Figure 7 also indicates the stars for which disk sizes have been measured (red symbols), where the dots indicate disk sizes >30 au and crosses indicate disks with sizes <30 au (Andrews et al. 2018a). It can be seen that most of these small disks are located in the relatively populated areas in Taurus, which agrees well with the expectations from our simulations. Possibly, close stellar flybys should not be excluded offhand as a cause for small disks in low-mass clusters.

In Section 4 we saw that close stellar flybys should lead to ≈13% of disks having sizes of ≤30 au. However, testing for the portion of small disk sizes alone is not sufficient, as these disks could equally just have formed small. However, there is a way to distinguish the two reasons for small disks. The relevant property is the disk’s outer edge. Disks that formed small should show a smooth decline in surface density all the way out. By contrast, truncated disks are distinguishable by their sharp outer edge (see Figure 8(c)). This distinct edge will eventually be smeared out owing to viscous spreading. However, it should be visible for at least 1–2 Myr. Therefore, the sharp outer edge should be most pronounced in relatively young clusters (<2 Myr), where viscous spreading has not had sufficient time to erase the sharp edge over this period.

External photoevaporation can also lead to disk truncation. The question arises whether small disks caused by external photoevaporation could be mistaken for those caused by close stellar flybys. Distinguishing small disks caused by flybys from those caused by external photoevaporation likely is not a major problem for two reasons. First, most low-mass clusters contain no O or B stars that could cause external photoevaporation. Second, the shapes of small disks produced by flybys and external photoevaporation differ considerably in their visual appearance. The best example for the disks that are affected by external photoevaporation are the proplyds in Orion (Ricci et al. 2008) with their tadpole shape (see Figure 8(a)). By contrast, flybys lead to the characteristic spiral arms (see Figure 8(b)) that quickly wind up, leaving behind a circular disk with a tightly wound ring structure (see Figure 8(c)). Thus, mistaking one for the other is quite unlikely.

The question arises why the influence of the environment in low-mass clusters has not become observationally apparent so far. Moreover, there are several studies showing that disk masses or frequencies in the centers of high-mass clusters like the ONC are lower than in the same cluster or in low-mass clusters (for a recent example, see van Terwisga et al. 2019), which is interpreted as the presence of environmental effects in these regions. However, using the evidence of environmental effects in high-mass clusters to conclude that environmental effects play no role in low-mass clusters, because so far no evidence of it has been found, would be a logical mistake. There are several reasons why so far the influence of the environment in low-mass clusters might not have become observationally apparent yet. First, there have been many dedicated observation campaigns to detect the effect of the environment in high-mass clusters, but none in low-mass clusters. When one does not expect an effect, the motivations to search for it are low. Second, in low-mass clusters, one always deals with small number statistics. Let us assume that in ONC-like clusters 5% of stars would be affected by the environment: this would still be a detectable effect, as it would concern 200 stars. For example, the prediction that the disk fraction or mass in the central area or close to the O stars is lower than elsewhere is relatively easy to test under these conditions. The
situation is quite different for low-mass clusters, where a 5% effect would concern 10 stars. Third, and perhaps most relevant, the cluster crossing time in the low-mass clusters investigated here is of the order of 0.1 Myr. Thus, in contrast to the situation in the high-mass clusters, these 10 affected stars would not be concentrated in the dense cluster center but could be anywhere within the cluster. Therefore, one would have to compare the disk masses in the entire area of high-mass clusters to that in low-mass clusters to determine the relative importance of environmental effects in dependence of cluster mass.

5.2. Planetary Systems

Close stellar flybys could affect resulting planetary disk structures in a variety of ways. What follows most directly from Sections 4 and 5 is that small truncated disks hinder the formation of planets on wide orbits. Especially planets on orbits that exceed 100 or 200 au should be less common than on smaller orbits. Unfortunately, currently there are still far too few known exoplanets on distant orbits to test this effect, as current exoplanet detection methods favor the detection of close-in planets. It is an open question whether most stars are formed in low- or high-mass clusters. However, as our model predicts that there is virtually no difference in the influence of low- and high-mass clusters on forming planetary systems, this result would hold independent of the outcome of this discussion.

The timescale of planet formation relative to cluster lifetime is still an open question. If planets do indeed form within 1–2 Myr, close flybys could influence directly the structure of the planetary system (Pfalzner et al. 2018; De Rosa & Kalas 2019; Winter et al. 2020). In this case, close stellar flybys primarily affect the outermost planets that form at the disk’s edge. Close stellar flybys during that stage would often excite those outer planets onto strongly eccentric orbits. A preference for outer planets showing eccentric orbits would be another indication of the relevance of close flybys.

A typical effect of a close flyby is the resulting spiral arm structure that quickly develops into eccentric rings that circularize on timescales of a few × 10^4 yr. Another sign for close stellar flybys in low-mass clusters would be a higher rate of structured disks among the small disks than the more extended disks in low-mass clusters. Close flybys could promote or accelerate planet formation in various ways also in small clusters. As flybys lead to the accumulation of material in these ring structures, this leads to localized higher dust densities, which is beneficial for dust growth. Similarly, close flybys can lead to gravitational instabilities that can trigger planet formation.

5.3. Cluster Dynamics

There is also a more indirect test of the above hypothesis. Low-mass clusters of the same size as high-mass clusters have a relaxation time of several tens of Myr after gas expulsion (see, e.g., Bastian & Goodwin 2006). Thus, these clusters would be well out of virial equilibrium at the age of 10 Myr. However, again this assumes that low- and high-mass clusters are of the same size. As observations tell us that this is not valid, and low-mass clusters are considerably smaller than high-mass clusters, low-mass clusters should already have reached virial equilibrium at ages of ≈5 Myr. Therefore, determining the velocity dispersion of low-mass clusters in the age range 5–15 Myr would allow testing the above assumptions. If the above model holds, low-mass clusters should already be close to virial equilibrium at 10 Myr.

6. From Low- to High-mass Clusters

In Section 4 we applied the commonly used method of studying the dynamics of young clusters starting out with a fully formed cluster. As mentioned in the introduction, this is done owing to the prohibitive computational expense of modeling the cluster formation process itself for a statistically significant number of cases. As pointed out, in this sense, our model has to be regarded as a toy model that does not account for the cluster formation process. Nevertheless, we try in the following to draw some conclusions concerning the close-flyby history during the star formation process, in particular for high-mass clusters.

Any cluster starts out with a small number of stars that gradually increases until the star formation process ceases, meaning that any high-mass cluster was once a low-mass cluster. The problem is that in the formation phase the clusters are still embedded in their gas. Therefore, their properties in terms of cluster mass and size are observationally much more
difficult to constrain. One could consider two scenarios for high-mass cluster formation, which might lead to different close-flyby histories.

First, high-mass clusters could already form spread out about a more extensive area from the start and only become identified as stellar overdensities when they have already reached a higher mass. In this case, their close encounter rate would gradually increase as the stellar density increases. Second, high-mass clusters could start small and become more extended later on, following the mass–radius relation. Then, high-mass clusters would undergo an early phase where they experience the same close stellar flyby history as low-mass clusters during later stages in their life. The only difference would be that the amount of gas would be higher. This second scenario might be the more realistic one, as the mass–radius relation seems to be obeyed independent of the gas mass of the cluster.

Although the close-flyby history differs in these two scenarios, the frequency of close encounters and the overall effect on the disks might be very similar. The difference lies more in the question of timing than inefficiency. In the first model, the frequency would steadily increase, be highest just before gas expulsion, and drop dramatically afterward. In the second model, the low- and high-mass clusters have a surprisingly similar frequency of close encounters. The close encounter rate would be more or less constant until gas expulsion. More observations of clusters in the deeply embedded phase are necessary to distinguish between the two options.

### 7. Summary and Conclusion

This study tests the hypothesis that close stellar flybys might be more common in young, low-mass, short-lived clusters (N ≈ 200) of the solar neighborhood than anticipated so far. Our approach is based on the observational correlation between an embedded cluster’s mass and size in the solar neighborhood’s stellar groups. We showed that the smaller size of low-mass clusters translates into a somewhat higher mean density than in high-mass clusters. Moreover, in low-mass clusters, not only is the mean density high, but the central stellar densities reach values above the threshold \( \rho = 10^4 \text{ pc}^{-3} \) for close stellar flybys affecting forming planetary systems. Motivated by our findings, we performed simulations of the dynamics in low- and high-mass clusters obeying the mass–size relation. We recorded the close-flyby history over the first 10 Myr of cluster development, and we find the following:

1. In low-mass clusters, close flybys seem to be as common as in high-mass clusters like the ONC. The mean occurrence rate and periastron distance of close flybys are similar in both environments.
2. In low-mass clusters, approximately 30% of the disks are truncated to 100 au or less in size. This disk truncation happens predominantly in the central areas of these clusters.
3. Amazingly, 13% of stars have flybys that lead to the truncation of their disk to less than 30 au. Thus, even in low-mass clusters, 13% of disks would be too small to form equivalents of the solar system because they would be either stripped of their outer planets or hindered from forming them in the first place.
4. Even in low-mass clusters, large disks with sizes of 1000 au or more have difficulties surviving. Half the stars in low-mass clusters have a flyby closer than 1500 au, corresponding to a truncation disk size of approx 500 au for an equal-mass encounter.

Thus, the cluster environment’s influence is relatively independent of the cluster’s mass or, equivalently, the number of stars in it. Only in clusters \( N > 10,000 \) or compact long-lived clusters predominantly found in the spiral arms or the galactic center are close flybys considerably more common than in the low-mass clusters investigated here.

If confirmed, these findings would require a paradigm shift in terms of the expectation of the relevance of close stellar flybys in low-mass clusters. So far, the expectation was that close stellar flybys are so rare in low-mass clusters that their effect on forming planetary systems is negligible. As a consequence, observations of low-mass clusters are nearly never checked for environmental influence. However, our results suggest that low-mass clusters influence a forming planetary system to the same degree as the ONC.

These theoretical results lead to three observationally testable predictions. First, as we saw, close stellar flybys should lead to ≈13% of disks having sizes of \( \leq 30 \) au. However, testing for the portion of small disk sizes alone is not sufficient, as these disks could equally just have formed small. The relevant property is the disk’s outer edge, which should be sharp in contrast to shallow outer edges of the disks that formed small. This sharp outer edge should be most pronounced in young clusters (\(<2\) Myr), as viscous spreading has not had sufficient time to erase the sharp edge over this period. Second, a preference of outermost planets on wide orbits (\(>20\) au) showing high eccentricity would be another indication of the relevance of close flybys even in low-mass clusters. Third, 10–20 Myr old low-mass clusters should be close to virial equilibrium.

### Appendix

In Section 4 we have shown that, taking the mass–radius relation into account, low-mass clusters have a small disk size as in the standard model V200. Figure A1 shows the disk size distribution for model V200 for comparison with Figure 5.

Figure A1. Disk size distribution for cluster K200. The bottom panel shows the size range from 0 to 1000 au, whereas the top panel displays a zoom-in on disks smaller than 100 au.
