Automatic Tuning of a Novel Ring Resonator-based Photonic Beamformer for a Transmit Phased Array Antenna

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Abstract—We present a novel photonic beamformer for a fully integrated transmit phased array antenna, together with an automatic procedure for tuning this system. Such an automatic tuning procedure is required because the large number of actuators makes manual tuning practically impossible. The antenna system is designed for the purpose of broadband aircraft-satellite communication in the Kᵢ-band to provide satellite Internet connections on board the aircraft. The goal of the beamformer is to automatically steer the transmit antenna electronically in the direction of the satellite. This is done using a mix of phase shifters and tunable optical delay lines, which are all integrated on a chip and laid out in a tree structure.

The Kᵢ-band has a bandwidth of 0.5 GHz. We show how an optical delay line is automatically configured over this bandwidth, providing a delay of approximately 0.4 ns. The tuning algorithm calculates the best actuator voltages based on past measurements. This is the first time that such an automatic tuning scheme is used on a photonic beamformer for this type of transmit phased array antenna. We show that the proposed method is able to provide accurate beamforming (< 11.25° phase error over the whole bandwidth) for two different delay settings.

Index Terms—microwave photonics, photonic beamforming, phased array antenna, automatic beamformer tuning

I. INTRODUCTION

Beamformers are used to steer the beam of a phased array antenna by controlling the phase added to the signal at each antenna element (AE) [1]. This can be done by providing either a phase shift or a time delay to the signal. When the phase or delay of the signal corresponding to each AE has been set correctly according to the desired beam angle, signals are received or transmitted in the desired direction, while other directions are suppressed. This results in a highly directional antenna system for which the beam angle can be adapted without any mechanical movement. See Figure 1 for the case of a transmit phased array antenna. A receive antenna uses the same principle, but in this work we only consider a transmit antenna.

In order to get the same signal to each AE with a certain delay, a beamformer for a transmit phased array antenna

This research was supported by the Dutch Technology Foundation STW under Project 13336.

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Fig. 1. Beamforming for a phased array antenna explained. Each antenna element transmits the same signal after a certain time delay. This delay can be chosen in such a way that constructive interference occurs in a certain direction, making it possible to transmit a highly directional signal with a high gain and a focused beam.
proposed phased array receiver [6] that is to be used in transmit mode. In order to tune the beamformer actuators of these earlier phased array antenna systems, either a manual tuning procedure was used [2], [3], which is only possible for a small number of actuators, or a nonlinear optimization algorithm based on a physical model of the system was used [4, Sec. 6]. However, the approach that uses a nonlinear optimization algorithm is very sensitive to model errors [7], requires a labor-intensive measurement procedure for certain parts of the physical model [4, App. B], and can not be used while the system is already running. In this work we describe the beamformer for the transmit phased array antenna from Figure 2 together with its requirements, and we show how to tune this system with a different optimization algorithm. This online algorithm is not sensitive to model errors and can be used while the system is running.

II. FULLY INTEGRATED TRANSMIT PHASED ARRAY ANTENNA

A. Beamformer requirements

In order to determine the requirements of the beamformer, the delay between the AEs needs to be calculated. This depends on two factors: the angle of the beam, and the distance between the AEs. For rectangular array grids, the latter should be equal to half the wavelength corresponding to the highest frequency used in the application [2, Sec. V], which is 14.5 GHz in this case. This leads to a distance of 1.03 cm between two consecutive AEs. As for the beam angle, this is chosen to be no more than 60 degrees compared to the normal (i.e. a beam sent straight upwards). The maximum delay $\tau_{\text{max}}$ that needs to be provided by each beamformer in Figure 2 can now be calculated as follows:

$$\tau_{\text{max}} = \sin(60^\circ) d_{\text{max}} / c_0,$$

where $d_{\text{max}}$ is the maximum distance between the centers of the different elements of the beamformer and $c_0$ is the speed of light. For the rightmost RF beamformer in Figure 2 $d_{\text{max}} = \sqrt{2} \cdot 0.0103$ m (distance between the centers of two diagonally intersecting AEs), for the other RF beamformer $d_{\text{max}} = 2 \cdot 0.0103$ m, for the $1 \times 4$ photonic beamformer $d_{\text{max}} = \sqrt{2} \cdot 4 \cdot 0.0103$ m, and for the $1 \times 4$ photonic beamformer $d_{\text{max}} = \sqrt{5^2 + 1^2} \cdot 0.0824$ m. This leads to the following maximum delays for each beamformer in Figure 2: $\tau_{\text{max}} = 42$ ps for the rightmost RF beamformer, $\tau_{\text{max}} = 84$ ps for the other RF beamformer, $\tau_{\text{max}} = 168$ ps for the $1 \times 4$ photonic beamformer, and $\tau_{\text{max}} = 1.214$ ns for the other photonic beamformer.

After calculating the maximum delays for each beamformer subsystem, the requirements for the phase can be calculated. The phase response of each beamformer should be a linear function of the frequency, with a slope equal to $-2\pi\tau$, where $\tau$ is the required delay. Traditionally, phase shifters are used for beamformer subsystems, which provide a phase shift that is a constant function of the frequency. In other words, phase shifters provide a linear phase response with a slope of 0. For very small delays (e.g. $\tau_{\text{max}} < 100$ ps in this case), using such
a constant phase response with a slope of 0 instead of $-2\pi \tau$ gives a negligible slope mismatch, but for larger delays this mismatch will have a negative influence on the antenna beam. This problem is called beam squint.

The effects of beam squint are negligible in the two RF beamformer subsystems in Figure 2. Therefore, these beamformers are based on phase shifters that change the phase of the RF signal. The photonic beamformers, however, need to deal with larger delays. Therefore, they make use of optical delay lines rather than phase shifters. The key principle here is that the RF signals are converted to the optical domain, where their phase is adjusted accordingly, and then they are converted back to RF domain. This combination of RF and photonic signal processing has many advantages such as low loss, low weight, and large bandwidth, especially when implemented on a chip [8]. In this work, each transmit tile from Figure 2 is connected to a corresponding chip, as explained later on in this section.

The way the photonic beamformers provide a linear phase response with the correct slope is by using a cascade of optical ring resonators as tunable optical delay lines, arranged in a tree structure [2], [8], [9]. These ring resonators control the phase response of the signal by using thermo-optic heater actuators. Though some fluctuations in the phase response are allowed, these fluctuations should not be larger than $11.25^\circ$ [3].

### B. Photonic beamformer chip design

Figure 3 shows the chip design of the photonic beamformers. The chip contains optical ring resonators that each belong to different subsystems. The effect of the different subsystems on the frequency response of the signal is shown as well. An RF splitter (subsystem 1 in Figure 3) makes sure that the same baseband signal arrives at all of the 24 transmit tiles shown in Figure 2. Each transmit tile is connected to one chip containing photonic and RF beamformer systems. The photonic beamformers use a combination of TriPleX™ waveguide technology [10] and indium phosphide (InP). TriPleX™ is a silicon nitride planar waveguide technology developed by LionX International.

The corresponding power response of the signal entering the chip in Figure 3 is that of a broadband signal centered around the frequency $f_{\text{RF}} = 14.25$ GHz in the Ku-band. This signal is modulated on an optical carrier with a Mach-Zehnder modulator (electrical-to-optical conversion), after which the optical signal consists of the carrier $f_c$ in the THz range and two sidebands. One of these sidebands is suppressed by the optical sideband filter (OSBF, subsystem 2 in Figure 3). This is done to reduce the required bandwidth [2]. After this stage the signal goes through a cascade of five ring resonators (subsystem 3 in Figure 3) that supply the required delay for one branch of the $1 \times 24$ beamformer. As mentioned earlier, the maximum delay that needs to be provided by the $1 \times 24$ beamformer is $\tau_{\text{max}} = 1.214$ ns. This should be no problem for a cascade of five ring resonators, as beamforming with a cascade of only three ring resonators has been illustrated for delays of more than 1.2 ns with a bandwidth of 0.5 GHz using a manual tuning approach [11].

The signal then arrives at a $1 \times 4$ optical beamforming network (OBFN, subsystem 4 in Figure 3), consisting of an optical splitter and more ring resonators. These ring resonators provide a linear phase response for a maximum delay of
168 ps, as calculated earlier in this section. As seen in the phase response in Figure 3, the linear phase response is only provided in the region of interest, the sideband around frequency \( f_c + f_{RF} \). However, the OBFN only makes sure that this linear phase response has the correct slope, not the correct absolute phase. The last subsystem (subsystem 5. in Figure 3) provides an additional phase shift so that the correct phase response is provided at the sideband and also at the carrier frequency \( f_c \). This is again done with optical ring resonators, using a principle called separate carrier tuning (SCT) [12]. Finally, the signal is converted back to RF domain with photodetectors (optical-to-electrical conversion).

The ring resonators in the beamformer subsystems are all actuated with two heaters: one for the phase, and one for the tunable coupling [13], [11]. By changing the voltages of these two heater actuators for several ring resonators, the magnitude and phase response of the subsystems can be altered. There are 27 ring resonators shown in Figure 3, resulting in 54 heaters. Three other heaters in the OBF sub-system and three heaters in the 1-to-4 splitter are not shown in the figure but increase the number of heaters to 60. So the total number of heaters in the two photonic beamformer stages is \( 24 \times 60 = 1440 \). One of the main reasons for investigating automatic procedures is that tuning all these heaters correctly by hand would not be practical.

III. AUTOMATIC TUNING RESULTS

A. Automatic tuning method

In this paper we look at an automatic tuning procedure for one branch of the OBFN subsystem. The traditional approach to automatically tune one branch of the photonic beamformer is to use a nonlinear optimization algorithm that minimizes a performance metric [4, Sec. 6]. An example performance metric is the mean square error (MSE) between the desired and actual phase response of the system \( \phi_D(f, V) \) and \( \phi_P(f, V) \) respectively:

\[
\min_V \sum_k (\phi_D(f_k, V) - \phi_P(f_k, V))^2. \tag{2}
\]

Here, \( V \) represents a vector of actuator voltages while the \( f_k \) represent the different frequencies that are relevant to the system. The actual phase response \( \phi_P(f, V) \) can be calculated from physical models of the heaters and optical ring resonators.

The procedure described above has several disadvantages. First of all, we have shown in earlier work that even very small errors in the physical model can have a large detrimental effect on the accuracy of the procedure [7]. Such model errors can never completely be avoided. Second, although physical models are available for each system component, the heater actuators influence each other by means of electrical and thermal crosstalk. This crosstalk can also be modeled, but this requires a number of measurements that is at least equal to the square of the number of heater actuators [4, App. B]. This becomes a problem when the number of heater actuators is large, and it gives even more room for model errors. Finally, the procedure has to be performed before actually running the system, and any changes to the system are not automatically taken into account.

To avoid the drawbacks mentioned above, recently automatic tuning algorithms based on machine learning techniques have been derived [7], [14], [15]. These algorithms use system measurements in the performance metric. Instead of calculating the phase response from physical models, the phase response is measured directly:

\[
\min_V \sum_k (\phi_D(f_k, V) - \phi_M(f_k, V))^2. \tag{3}
\]

Here, \( \phi_M(f, V) \) denotes the measured phase response. This data-based algorithm learns the relation between the actuator voltages and the performance metric in (3) and chooses those voltages that optimize this metric. After several iterations, the algorithm converges to a setting of actuator voltages \( V \) with the best performance according to the data-based performance metric [5]. Here, each iteration consists of updating the performance metric with the measured phase response, finding the optimal values for \( V \), and setting the actuator voltages to these values and performing a new measurement. In this work this is done with the data-based online extremum-seeker (DONE) algorithm [14]. See Figure 4. This algorithm is especially designed for systems where the measurements take some time to be performed, where measurement noise is present, and where the relation between the MSE and the actuators is too complicated to model accurately. The beamformer system described in this paper is an example of such a system. Using such an automatic tuning procedure on this system with over a thousand actuators is unavoidable if it is ever to be used in a real life application. Besides this, the DONE algorithm only uses the MSE in (5), which is a scalar value. This makes it easy to be used in practice, where it is more realistic to use a scalar value as the objective, for example by measuring the signal-to-noise ratio or output power of the system rather than the phase response. The traditional approach with the nonlinear optimization method also uses a scalar-valued objective, but it becomes very slow and struggles with local minima when the output power is used as the objective [16, Sec. 4.4.2].
Unlike the traditional approach \cite{2}, the data-based approach \cite{1} does not require a physical model (including a model for the heater crosstalk) and is therefore not sensitive to model errors. It is also an online algorithm, which means that it can be used while the system is running, and it will continually search for better configurations. This can also easily be adapted to allow the procedure to work for systems that change over time, which is crucial when applied to antenna systems on moving vehicles such as aircrafts. On moving vehicles, the beam angle changes over time, and therefore the objective function also changes over time.

B. Optical sideband filter tuning

Earlier in this paper, several subsystems of the photonic beamformer were described. See Figure 3. The OSBF and SCT subsystems drastically reduce the required bandwidth of the system \cite{2, 12}. The goal of the OSBF is to filter out one of the sidebands resulting from the modulation scheme used for the E/O conversion, as shown in the frequency responses of Figure 3. The result is an optical single sideband full carrier modulation that can be used by the OBFN. With one sideband filtered out, beamforming would need to be performed over the sideband, the optical carrier frequency, and the frequencies in between, giving a total of 14.5 GHz instead of the whole region of 29 GHz. To further reduce the bandwidth, the SCT subsystem is used to ensure that the correct phase is achieved at the carrier frequency. If both the OSBF and SCT subsystems are tuned correctly, a linear phase response only needs to be provided in one sideband with a bandwidth of 0.5 GHz.

Figure 5 shows the power response of the full beamformer system after tuning the OSBF subsystem by hand. This was done by measuring the power response with a vector network analyzer (VNA) and tuning the OSBF heaters until the desired response was achieved. The shown frequencies are relative to the carrier frequency. The response features a stopband, the optical carrier frequency, and the frequencies between, giving a total of 14.5 GHz instead of the whole region of 29 GHz. To further reduce the bandwidth, the SCT subsystem is used to ensure that the correct phase is achieved at the carrier frequency. If both the OSBF and SCT subsystems are tuned correctly, a linear phase response only needs to be provided in one sideband with a bandwidth of 0.5 GHz.

Figure 5 shows the power response of the full beamformer system after tuning the OSBF subsystem by hand. This was done by measuring the power response with a vector network analyzer (VNA) and tuning the OSBF heaters until the desired response was achieved. The shown frequencies are relative to the carrier frequency. The response features a stopband, that filters out one of the sidebands as shown in Figure 3 and a passband that keeps the other sideband. The difference between the stopband and passband is 30dB. In this work it is assumed that the RF signals are downconverted as in earlier work \cite{3, 6}, such that the sidebands are located closer to the carrier frequency than the 14.25 GHz mentioned earlier, though the results in this paper still hold for a bandwidth of 0.5 GHz.

C. Automatic optical beamforming network tuning

The optical beamforming network (OBFN) subsystem is used to provide different delays to the signals of each antenna element in such a way that a strong signal is transmitted in one specific direction by positive interference. The correct delays can be calculated from the desired beam angle and the distance between two antenna elements, as shown in the introduction. This leads to a maximum delay of 168 ps for the 1 × 4 photonic beamformer, which is the one investigated in this work. Larger delay values were considered in this work to show that the maximum delays can indeed be achieved, to allow different antenna configurations or scan angles, and for better visibility of the measurements.

The desired group delay response for each OBFN path is a flat response with a value between 0 ps and the maximum group delay value, depending on the desired beam angle. The group delay response can be made flat by using a serial configuration of ORRs for each OBFN path \cite{11}. This flat response has to be provided over the whole frequency range of interest. However, by implementing the SCT scheme explained later in this section, the only part of the frequency domain for which a flat group delay response needs to be provided is the sideband that is not filtered by the OSBF, as shown in Fig. 5. This greatly reduces the required number of ORRs and therefore the complexity of the system, because there is a trade-off between the required number of ORRs, the maximum group delay, and the bandwidth \cite{2}.

The procedure for tuning the OBFN is similar to the one for tuning the OSBF: the group delay response is measured with a VNA, and the heaters of each ring resonator are tuned until the desired group delay response is achieved. Here, we made use of the automatic tuning method described in this paper. The top of Figure 6 shows the resulting phase response of both the manual and the automatic tuning procedures of one path of the photonic beamformer system for two different delay settings (250 ps and 408 ps). The 1-to-4 splitter shown in Figure 5 has been set to provide this path with 100% of the signal power. In the automatic procedure, the frequency range where a linear phase response should be achieved was set to 4.5-8.1 GHz, which corresponds to a much larger bandwidth than the desired bandwidth of 0.5 GHz. The manual tuning approach used a frequency range of the same bandwidth but no specific frequency range was given. All results were time averaged to reduce noise.

The difference between the desired and the measured phase response must remain within 11.25°. The maximum errors are shown in Table 1. As can be seen, all phase errors remain well within the requirements. This shows that the automatic tuning procedure can be used instead of the manual tuning procedure for the photonic beamformer system.

The bottom of Figure 6 shows the corresponding power response. For the manual tuning method this is similar to the one
optical ring resonators. Two ring resonators are tuned in such a way that they affect the phase response in the region between the carrier frequency and the sideband. This region contains no information, so it is not necessary to follow the desired linear phase response here. Tuning these two ring resonators gives an extra phase shift while leaving the shape and the slope of the phase response unaffected. This ensures that the phase response follows the desired linear phase response at the carrier frequency too. It should be noted that phase differences of multiples of $360^\circ$ do not affect the system [12]. This makes it theoretically possible to use only one ring resonator for this adjustment, though in practice it is easier to use two of them. The ring resonators in the SCT subsystem were adjusted by hand after tuning their heater actuators in such a way that the ring resonators only operate in the region near the carrier frequency.

Figure 7 shows the effect of not using the SCT subsystem on the left. Although the phase response has the desired slope, there is a phase mismatch at the carrier frequency (at 0 GHz). Tuning the ring resonators of the SCT subsystem solves this problem. The effect of tuning the SCT subsystem is shown in the same figure on the right. This time, the phase responses have been shifted up or down in such a way that the corresponding linear phase responses are a multiple of 360 degrees off at the carrier frequency. The accuracy can still be improved, however: due to their proximity on the photonic chip, the heaters of the SCT subsystem slightly influence the heaters of the OBFN subsystem, which leads to small changes to the slope of the phase response. This causes the desired phase response at the carrier to be about 30 degrees off, so exact multiples of 360 degrees are not yet achieved. These errors are unacceptable for practical applications. However, using the same automatic tuning procedure for this subsystem together with the other two subsystems could circumvent this problem. This remains for future work.

### Table I

| Delay   | Method | Max error |
|---------|--------|-----------|
| 408 ps  | (M)    | 6.2°      |
| 250 ps  | (M)    | 4.9°      |
| 408 ps  | (A)    | 5.5°      |
| 250 ps  | (A)    | 6.4°      |

Maximum phase error in degrees for tuning the OBFN subsystem automatically (A) and by hand (M) for different delay values. All errors are well below the maximum allowed error of 11.25°.
Fig. 7. Measured phase response of the full beamformer system before (left) and after (right) manually tuning the SCT subsystem. The word ‘auto’ in the legend refers to the automatic tuning of the OSBF and OBFN subsystems. Using the SCT principle, the height of the phase responses is adapted in such a way that the corresponding linear responses meet at the carrier frequency, up to multiples of 360 degrees, as indicated by the red circles. These results have also been published in [17].

IV. Conclusion

We have proposed a novel photonic beamformer for a transmit phased array antenna. The beamformer is based on optical ring resonators and is fully integrated on a chip. We have investigated manual and automatic procedures for tuning the photonic beamformer. Automatic procedures are essential in real-life applications where thousands of actuators are considered and where a limited number of variables can be measured, such as the signal-to-noise ratio. Both the manual and automatic procedures provided beamforming functionalities with a phase error of less than 11.25° over the whole frequency band that contains signal information. This is the first time that part of this transmit antenna tile has been tuned automatically.

The system is designed with aircraft-satellite communication in mind as the main application, providing satellite Internet connections on board the aircraft using the K_{u}-band. The separate carrier tuning principle greatly reduces the operating bandwidth for the photonic beamformer, from 29 GHz to 0.5 GHz. The ring resonator-based subsystems of the beamformer make squint-free beamforming possible. A fully automated transmit antenna tile remains for future work.

Appendix A

Measurement Setup

Figure 8 shows the measurement set-up for the frequency response measurements shown in this paper. A Rohde& Schwarz ZVA40 VNA generated a 50 MHz RF signal to modulate a laser with a Mach-Zehnder modulator. The modulated optical signal was coupled into the beamformer control box. The control box was connected via USB to a laptop with heater control software. This laptop also contained the automatic tuning software and software for reading the VNA measurements. The integrated photodetectors inside the control box were connected with RF cables to the second VNA port. Although integrated modulators were also available, these have not been used in order to prevent crosstalk with the integrated detectors.

The VNA measurements were sent to the laptop with the automatic tuning and heater control software via an ethernet cable. The phase-shift method [3, Sec. IV-A] was used for the group delay and power response measurements, using a function generator for the laser. With this method, the phase response shown on the VNA is actually equivalent to the group delay response of the system, so the objective (3) minimized by the DONE algorithm is actually equal to the mean square error between the desired and measured group delay response. In Figures 6 and 7, after the minimization procedure, the phase response was measured directly using a frequency sweep on the VNA (without the external trigger from the function generator). Here, the laser current was chosen in such a way that the optical carrier would be at 0 GHz in Figure 5 after tuning the OSBF.

Appendix B

Algorithm Settings

The automatic tuning algorithm used in this paper contains several hyper-parameters that are explained and investigated in [14]. Their values as used in this paper are shown in Table II for the OSBF and OBFN tuning results. The last value indicates the size of the sliding window: only the last 60 measurements are used in updating the model used by the algorithm, using the same adaptation of the algorithm as in [18].

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Fig. 8. Measurement set-up for the frequency response measurements used in this paper.

| Hyper-parameter                  | Value (OSBF tuning) | Value (OBFN tuning) |
|----------------------------------|---------------------|---------------------|
| Total num. of measurements       | 2000                | 1000                |
| Num. of basis functions          | 3000                | 3000                |
| Regularization parameter         | 0.1                 | 0.1                 |
| Standard deviation of frequencies | 1.0                 | 1.0                 |
| Exploration parameter            | 0.03                | 0.05                |
| Sliding window size               | 60                  | 60                  |

TABLE II
VALUES OF THE HYPER-PARAMETERS USED BY THE AUTOMATIC TUNING ALGORITHM.

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