Contribution of the Determination of the Load on Suspension Ring of the Underframe of the Hydraulic Excavator

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In this paper it is presented a method for determining the load on the suspension ring of underframe of hydraulic excavator which binds radial-axial bearing. The approach is based on the use of Kane's equations with undetermined multipliers of constraints. The expressions are derived in symbolic form for the forces which suspension ring is exposed during the operation of digging. In addition to the kinematic and inertial parameters of the excavator, in these expressions are included the forces in hydro cylinders as well as parameters that characterize the operation of digging. For specific numerical values of the system parameters, numerical analysis is carried out and the appropriate load graphics are presented.

Keywords: Hydraulic excavator, Suspension ring, Multibody, Dynamics

0. INTRODUCTION

Excavators are universal construction machines with cyclic work, which primary task is excavation of soil, and the secondary is transport of excavation to the place of disposal or loading in appropriate transportation means. Their working cycle consists of: digging of soil with the bucket filling, the bucket lifting, transfer of excavated material to the place of discharge, bucket discharge and taking up the original position.

Excavator (Figure 1) consists of the basic machine and excavation device. The basic machine consists of running gear device and rotating part of machine, while the excavator device is composed of boom, bucket stick and bucket. Depending on type of the running gear device there are two types of excavators: wheel excavators and crawler excavators which are most common in the application.

Crawler excavators are self-propelled machines, whose running gear device allows moving the excavator from one to another place of excavation, while not performing transport of excavated material. The running gear device of excavator consists of frame, caterpillar running gear machine and mechanism for drive and braking. Caterpillar tracks have independent drive by individual hydraulic motors by a system mechanical transmission, thereby providing a synchronized or separated movement of the caterpillar tracks.

Rotating platform is the basic metal construction of the excavator, on which are mounted working device, hydraulic drive, cabin with driving system and rotating mechanism. The main objective of placement of devices on rotating platform is achievement of best static moment, by which it prevents the overturning of the excavator. For that reason, on rotary platform is placed the counterweight. Rotating platform with rotating-supporting ring is connected with running gear machine, and thus own and working loads that acting on working device during operation, are transferred to the ground.

The underframe is integral part of the running gear device of the excavator and it represents one of the most important parts of the supporting structure of the excavator.

Its main task is to transfer the load from the upper frame, by slewing bearing on mechanism for movement. Support ring represents a part of underframe which binds to slewing bearing. It is usually welded structure made from sheet metal, whose elements are made by cutting and folding.

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Besides transferring the load, slewing bearing have task to ensure the stability and to allow undisturbed functioning of the rotating part of excavator. This bearing is made in the form of one or more rows of balls or rollers, with gearing on the bearing ring which is connected to functioning of the rotating part of excavator. This bearing have task to ensure the stability and to allow undisturbed exploitation parameters.

The mass centres of bodies \((V_i)\) \((i = 0,1,...,4)\) are denoted by \(C_i\). According to \([2,3]\), the transformation matrix \(A_{ij}\) \((i = 0,...,4; j = 1,...,4)\) from \(O_j\xi_j\eta_j\zeta_j\) to \(O_i\xi_i\eta_i\zeta_i\) reference frames \((i = 0)\) corresponds to the frame \(C_{0\xi_0\eta_0\zeta_0}\) has the form:

\[
A_{ij} = \prod_{k=i+1}^{j} A_k^i = \prod_{k=i+1}^{j} (I + (1 - \cos q_k)(\hat{e}_k^{(k)})^2 + \hat{e}_k^{(k)}\hat{e}_k^{(k)\top}), 1 < j,
\]

where \(A_k^i \in R^{3 \times 3}\) is the Rodriguez matrix \([2]\), \(I \in R^{3 \times 3}\) is the identity matrix, and \(\hat{e}_k^{(k)} \in R^{3 \times 3}\) is the skew symmetric matrix \([2,4]\) associated with the vector \(e_k^{(k)}\).

In further considerations the right superscript \((k)\) indicates that components of the corresponding vectors and matrices are given in the \(O_k\xi_k\eta_k\zeta_k\) local frame. In regard to \([5,6]\), the following kinematic relations of the considering hydraulic excavator hold \([1]\):

\[
\omega_k^{(i)} = \omega_{yi}^{(i)} + \hat{a}_i \cdot \omega_{yi}^{(i)}, i = 1,...,4 \tag{2}
\]

\[
e_k^{(i)} = \omega_{yi}^{(i)} + \hat{a}_i \cdot \omega_{yi}^{(i)} + \hat{q}_i \cdot \omega_{yi}^{(i)} + \hat{a}_i \cdot a^{(i)}_i + \omega_{yi}^{(i)} \cdot a^{(i)}_i, i = 1,...,4 \tag{3}
\]

\[
V_{C_i}^{(i)} = \omega_{yi}^{(i)} \cdot (V_{C_i}^{(i)} + \hat{a}_i \cdot a^{(i)}_i + \omega_{yi}^{(i)} \cdot a^{(i)}_i) + \omega_{yi}^{(i)} \cdot a^{(i)}_i, i = 1,...,4 \tag{4}
\]

\[
a_k^{(i)} = \omega_{yi}^{(i)} \cdot (V_{C_i}^{(i)} + \hat{a}_i \cdot a^{(i)}_i + \omega_{yi}^{(i)} \cdot a^{(i)}_i) + \omega_{yi}^{(i)} \cdot a^{(i)}_i, i = 1,...,4 \tag{5}
\]

where \(\omega_k^{(i)}, e_k^{(i)}\) and \(a_k^{(i)}\) are, respectively, the angular velocity, the angular accelerations, the velocity of the mass centre \(C_i\) and the acceleration of the mass centre of body \((V_i)\), and where \(l_i = \left|\overline{O_iC_i}\right| (i = 1,...,3)\), \(l_0 = \left|\overline{C_0O_0}\right|\), \(l_C = \left|\overline{O_iC_i}\right| (i = 1,...,4)\), and \(l_{c0} = [0,0,0]^T\).

Since the body \((V_0)\) is immovable, the following holds:

\[
V_{C_0}^{(0)} = [0,0,0]^T, \quad a_{C_0}^{(0)} = [0,0,0]^T. \tag{6}
\]
2. DETERMINATION OF THE LOAD ON SUSPENSION RING OF THE UNDERFRAME DURING THE DIGGING TRANSPORTATION TASK

The interaction between the bucket and the soil during the excavation phase is shown in Figure 4. The digging force $F_W$ acts on the centre $K$ of the cutting edge of the bucket. The force $F_W$ depends on various factors such as the depth of the bucket tip $K$, the width of the bucket, the terrain slope, and the soil physical characteristics. Different expressions for the magnitude of the force $F_W$ can be found in [7,8,9,10]. The digging angle is denoted by $\theta_b$ and $\theta_d$ represents the angle between the bucket bottom and the $\eta_4$ - axis. In regard to [7,11], the angle $\delta$ varies in the interval $0.1 \leq \delta \leq 0.45$ and depends on the digging angle, digging condition, and the wear of the bucket cutting edge. As in [7,11,12], in this paper it is taken that this angle is constant and equal to $\delta = 0.1$.

In accordance with Figure 4, the force $F_W$ can be written as

$$F_W^{(4)} = [0, -F_W \cos(\delta + \theta_b), F_W \sin(\delta + \theta_b)]^T.$$  

The moment of the force $F_W$ relative to point $C_4$ is determined by the following expression:

$$M_4^{(4)} = -\vec{F}_W^{(4)}(O_4K^{(4)} - I^{(4)}_C).$$  

Hence, the external force system exerted on bucket can be represented by a force system consisting of a force equal to $F_W$ that passing through the mass centre $C_4$, the gravity force $m_4g$ of the bucket, and a couple with torque $M_4$.

Based on approach from [14], the load of the suspension ring can be represented by a force passing through the point $O^*$:

$$R^* = [\lambda_1, \lambda_2, \lambda_3]^T$$

and a couple with torque

$$M^* = [\lambda_4, \lambda_5]$$

where $\lambda_i$ ($i = 1,...,5$) are the projections of the vectors $R^*$ and $M^*$ onto the corresponding axes of the frame $O^*\xi^*\eta^*\zeta^*$.

Based on [14], these projections are determined by the following expressions:

$$\lambda_i = \sum_{p=1}^3 \left[ F_p^{(p)} \omega_{p,r}^{(p)} b_p^{(p)} + (M_p^{(p)})^T b_p^{(p)} \right] - m_p \omega_{C_p}^{(p)} \omega_{C_p}^{(p)} - \sum_{r=1}^5 (I_{C_p} x_p^{(p)} + \omega_p^{(p)} I_{C_p} \omega_p^{(p)})^T b_p^{(p)}, r = 1,...,5$$

where it is taken that an external force system exerted on body $(V_p)$ ($p = 1,...,3$) is represented by an equivalent force system consisting of a force $F_p$ passing through the mass centre $C_p$ together with a couple with torque $M_p$.

In Eq. (11), $I_{C_p}$ represents the centroidal inertia tensor of the body $(V_p)$ expressed in the local frame $C_p\xi_p\eta_p\zeta_p$ whose axes are chosen so that $C_p\xi_p \parallel O_p\xi_p$, $C_p\eta_p \parallel O_p\eta_p$ and $C_p\zeta_p \parallel O_p\zeta_p$ hold.
Taking this into account, the projections of vectors in both coordinate frames \( C_p \bar{e}_p \bar{p}_p \bar{p}_p \) and 
\( O_p \bar{e}_p \bar{p}_p \bar{p}_p \) are the same.

Based on the considerations in [14], the vectors \( b_{p,r}^{(p)} \) and \( b_{p,s}^{(p)} \) are determined by the following expressions:

\[
b_{p,r}^{(p)} = \begin{cases} 
[0,0,0]^T, r = 1, 2, 3; p = 1, \ldots, 4 \\
A_{p}^{(p)}[1,0,0]^T, r = 4; p = 1, \ldots, 4 \\
A_{p}^{(p)}[0,1,0]^T, r = 5; p = 1, \ldots, 4 \\
\end{cases}
\]

\[
b_{p,s}^{(p)} = \begin{cases} 
A_{p}^{(p)}[1,0,0]^T, r = 1; p = 1, \ldots, 4 \\
A_{p}^{(p)}[0,1,0]^T, r = 2; p = 1, \ldots, 4 \\
A_{p}^{(p)}[0,0,1]^T, r = 3; p = 1, \ldots, 4 \\
\end{cases}
\]

(12)

- \( \varepsilon_{ij}^{(p)} \):
\[
\varepsilon_{ij}^{(p)}(\lambda) = A_{ij}^{(p)} O_i O_j + F_{ij}^{(p)} + \sum_{j=1}^{n} A_{ij}^{(p)} F_{ij}^{(p)}
\]

(13)

where:
\[
\varepsilon_{ij}^{(p)} = A_{ij}^{(p)}[1,0,0]^T \\
\varepsilon_{ij}^{(p)} = A_{ij}^{(p)}[0,1,0]^T \\
\overrightarrow{O_i} = [0,0,0]^T \\
\overrightarrow{O_j} = [0,0,0]^T
\]

(14)

3. NUMERICAL EXAMPLE

For purposes of determining the numerical values of projections \( \lambda_i \) (\( i = 1, \ldots, 5 \)) the following values of the excavator parameters are used (see [7, 11, 12]):

- \( m_1 = 6420 \text{ kg}, \quad m_2 = 1566 \text{ kg}, \quad m_3 = 735 \text{ kg}, \quad m_4 = 432 \text{ kg}, \quad I_{C_2} = 14250.6 \text{ kg m}^2, \quad I_{C_4} = 727.7 \text{ kg m}^2, \quad I_{C_4} = 224.6 \text{ kg m}^2, \quad I_{C_4} = 25.9 \text{ m}, \quad l_1 = 0.05 \text{ m}, \quad l_2 = 5.16 \text{ m}, \quad l_3 = 2.59 \text{ m}, \quad \overrightarrow{O_4} = 1.33 \text{ m}, \quad \overrightarrow{O_1} = 0.76 \text{ m}, \quad l_{C_1} = 0.61 \text{ m}, \quad l_{C_2} = 2.71 \text{ m}, \quad l_{C_3} = 0.64 \text{ m}, \quad l_{C_4} = 0.65 \text{ m}, \quad \gamma_4 = 1.92, \quad \angle(I_{C_1}, \eta_1) = 3.49305, \quad \angle(I_{C_2}, \eta_2) = 0.2566, \quad \angle(I_{C_3}, \eta_3) = 0.3316, \quad \angle(I_{C_4}, \eta_4) = 0.3944, \quad \theta_b = 1.0472.

The quantities \( I_{C_i} \) (\( i = 2, 3, 4 \)) represent second-order inertial moments about the axes through the gravity centres \( C_p \bar{e}_p \bar{p}_p \bar{p}_p \) (\( p = 2, 3, 4 \)), respectively. At that, as in [13], it is taken that the time interval of the considered digging task reads \( 0 \leq t \leq 3 \text{ s} \) and that:

\[
q_1(t) = 0, \quad q_2(t) = -0.1744, \quad q_3(t) = 0.436, \quad q_4(t) = -0.1744t^3 - 0.7848t^2
\]

and

\[
F_w(t) = 2.812t^3 - 18.097t^2 + 35.9936t [\text{kN}].
\]

The external force systems acting on the bodies \( (V_i) \) (\( i = 1, \ldots, 4 \)) are defined as follows:

\[
F_i^{(i)} = A_{i}^{(i)}[0,0,-m_4g]^T, \quad i = 1, 2, 3
\]

(17)

\[
F_4^{(4)} = [0,-F_w \cos(\delta + \theta_b), F_w \sin(\delta + \theta_b)] + A_{i}^{(i)}[0,0,-m_4g]^T
\]

(18)

and \( M_4^{(4)} \) is defined by the relation (8).

The graphs of the magnitude of the force \( F_w \) and projections \( \lambda_2, \lambda_3 \) and \( \lambda_4 \) are shown in Figs. 5, 6, 7, 8.

\[
\text{Figure 5: Magnitude of resistance digging (cutting) force } F_w \text{ versus time}
\]

\[
\text{Figure 6: The projection } \lambda_3 \text{ of the force } R \text{ onto the axis } O^* \eta^*
\]

\[
\text{Figure 7: The projection } \lambda_4 \text{ of the force } R \text{ onto the axis } O^* \zeta^*
\]
For the considering digging transportation task, the following holds:

\[ \dot{\lambda}_1(t) = 0, \]

\[ \dot{\lambda}_2(t) = 0. \]  

4. CONCLUSIONS

In this paper, expressions in symbolic form for projections of the force \( \mathbf{R}^* \) and the moment of couple of forces \( \mathbf{M}^* \), which is exposed to suspension ring of the underframe, are presented. These expressions allow to during the excavation phase examine the effect of various design parameters of excavator and the relevant factors in process of interaction between the bucket and the soil to the load of the suspension ring. The expressions (12) – (13) can be used also in the caselifting and returning transport operations. Approach from paper [14] allows the loading of the suspension ring be determined without the need for determining reaction forces in joints \( O_2, O_3 \) it \( O_4 \), so that in meaning of computation is superior in regard to the Newton-Euler approach [15].

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