CLASSIFYING SUPERNOVAE USING ONLY GALAXY DATA

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ABSTRACT

We present a new method for probabilistically classifying supernovae (SNe) without using SN spectral or photometric data. Unlike all previous studies to classify SNe without spectra, this technique does not use any SN photometry. Instead, the method relies on host-galaxy data. We build upon the well-known correlations between SN classes and host-galaxy properties, specifically that core-collapse SNe rarely occur in red, luminous, or early-type galaxies. Using the nearly spectroscopically complete Lick Observatory Supernova Search sample of SNe, we determine SN fractions as a function of host-galaxy properties. Using these data as inputs, we construct a Bayesian method for determining the probability that an SN is of a particular class. This method improves a common classification figure of merit by a factor of \( >2 \), comparable to the best light-curve classification techniques. Of the galaxy properties examined, morphology provides the most discriminating information. We further validate this method using SN samples from the Sloan Digital Sky Survey and the Palomar Transient Factory. We demonstrate that this method has wide-ranging applications, including separating different subclasses of SNe and determining the probability that an SN is of a particular class before photometry or even spectra can. Since this method uses completely independent data from light-curve techniques, there is potential to further improve the overall purity and completeness of SN samples and to test systematic biases of the light-curve techniques. Further enhancements to the host-galaxy method, including additional host-galaxy properties, combination with light-curve methods, and hybrid methods, should further improve the quality of SN samples from past, current, and future transient surveys.

Key words: galaxies: general – methods: statistical – supernovae: general

Online-only material: color figures

1. INTRODUCTION

Supernovae (SNe) are the result of several different kinds of explosions from different stellar progenitor systems. Separating SNe into different classes (or “types”) has existed for over 70 yr (Minkowski 1941). Despite the recent discovery of several new varieties of SNe (e.g., Foley et al. 2013), most SNe discovered can be placed into the two broad categories of “core-collapse (CC)” SNe (those with a massive star progenitor, corresponding to the Ib, Ic, II, IIn, and Ia classes) and Type Ia SNe (SNe Ia). Filippenko (1997) reviews the observational characteristics of these more common classes. There remain a few additional SNe that do not fall into these two categories, but these are a small fraction of the SNe discovered (Li et al. 2011).

Current transient surveys discover many more SNe than can be spectroscopically classified. Future surveys will have even lower rates of spectroscopic classification. Because of this limitation, there has been a significant amount of effort to photometrically classify SNe (see Kessler et al. 2010 for a review). Providing large and pure samples of individual classes of SNe is important for many studies. In particular, large samples of SNe Ia are required to make progress in determining the nature of dark energy (e.g., Campbell et al. 2013), driving cosmic acceleration, which was originally discovered through measurements of (mostly) spectroscopically confirmed SNe Ia (Riess et al. 1998; Perlmutter et al. 1999). Additionally, having some preliminary classification to aid in spectroscopic follow-up can be useful for studies of all classes of SNe.

Until now all effort has focused on classification using only the light curves of the SNe. Specifically, different SN classes tend to have different rise times, decline rates, and colors. Additionally, all efforts have focused on separating SNe Ia from all other types of SNe. This problem becomes more difficult with low signal-to-noise ratio data, sparse sampling, a sample that extends over a large redshift range, and limited filters. Nonetheless, the best photometric classification methods for a simulated SN sample are 96% pure while recovering 79% of all SNe Ia (Kessler et al. 2010; Sako et al. 2011; Campbell et al. 2013).

Our approach here is to classify SNe without using any SN photometry. This method uses the known correlations between host-galaxy properties and SN classes. Since CC SNe (SNe Ib and II) have massive star progenitors and SNe Ia have WD progenitors, several host-galaxy properties are correlated with SN type. For decades, we have known that CC SNe explode almost exclusively in late-type galaxies and are associated with spiral arms and H\(\text{II} \) regions. On the other hand, SNe Ia explode in all types of galaxies and have no preference for exploding near spiral arms. These basic facts drive the majority of our exploration.

Most of the host-galaxy data we use should be available for all transient surveys. We do not attempt to combine this classification technique with photometric classifications (or attempt hybrid approaches), and we leave such implementation to future studies.

The manuscript is structured in the following way. Section 2 describes a figure of merit (FoM) for determining the quality of classification. We introduce our SN samples in Section 3 and discuss host-galaxy properties in Section 4. Our method is described in Section 5, and we test the method in Section 6. We discuss our results, additional applications, and future prospects in Section 7 and conclude in Section 8.
2. FIGURE OF MERIT

When evaluating non-spectroscopic identification techniques, one needs a metric for comparison. Kessler et al. (2010) present an FoM for such a comparison, with the focus on producing a large sample of SNe Ia with low contamination. The FoM, \( \epsilon_{\text{IA}} \), is the product of the efficiency and pseudopurity of a sample of SNe classified as SNe Ia. The efficiency is defined as

\[
\epsilon_{\text{IA}} = \frac{N_{\text{IA}}^{\text{Sub}}}{N_{\text{IA}}^{\text{Tot}}},
\]

where \( N_{\text{IA}}^{\text{Tot}} \) is the total true number of SNe Ia in the full sample and \( N_{\text{IA}}^{\text{Sub}} \) is the true number of SNe Ia in a subsample classified as SNe Ia under some criterion. The pseudopurity is defined as

\[
PP_{\text{IA}} = \frac{N_{\text{IA}}^{\text{Sub}}}{N_{\text{IA}}^{\text{Sub}} + W_{\text{IA}}^{\text{False}} \cdot N_{\text{Non-IA}}^{\text{Sub}}},
\]

where \( N_{\text{Non-IA}}^{\text{Sub}} \) is the number of objects misclassified as SNe Ia in the selected subsample that are not truly SNe Ia, and \( W_{\text{IA}}^{\text{False}} \) is the weight given to adjust the importance of purity on the FoM. If \( W_{\text{IA}}^{\text{False}} = 1 \), the pseudopurity is simply the true purity, which is equivalent to the probability of an SN in that subsample being an SN Ia. Campbell et al. (2013) suggest that \( W_{\text{IA}}^{\text{False}} = 5 \) is the preferred value for creating a sample of SNe Ia for the purpose of measuring cosmological parameters; we will use that value throughout this paper.

If one can perfectly reject non-transient sources from the subsample, then \( N_{\text{Non-IA}}^{\text{Sub}} \approx N_{\text{CC}}^{\text{Sub}} \), where \( N_{\text{CC}} \) is the number of CC SNe in the subsample (there will perhaps be a few peculiar thermonuclear SNe in the subsample, but those will likely be orders of magnitude smaller than the CC population).

Of course, this FoM is not the only way to compare classification methods, and it is particularly focused on selecting a relatively pure sample of SNe Ia. But since we hope to merely provide practical and useful methods of classification for various surveys, there is no urgent need to define a different FoM. Regardless of whether one is trying to select SNe Ia or CC or wants to somehow weight efficiency and/or purity differently, the Kessler et al. (2010) FoM will likely still be informative.

3. DATA

3.1. Supernova Samples

When testing various classification schemes, one would ideally have a large, unbiased, spectroscopically complete sample. Unfortunately, this sample does not exist. Instead, previous studies have typically simulated large samples of SNe with the simulated sample properties matching those believed to be representative of a particular survey (e.g., Kessler et al. 2010). This approach is reasonable when generating samples of SN light curves since there is a significant amount of light-curve data available and sufficient understanding of the relative rates of various SN (sub)types and their luminosity functions (Li et al. 2011).

However, simulations are not necessarily appropriate when looking at host-galaxy properties of SN samples. Some observables have not been examined in detail, and the correlations between properties are not well understood. For the purposes of this examination, there is a large, almost spectroscopically complete sample of SNe that is relatively free of bias: the Lick Observatory Supernova Search (LOSS) sample (Leaman et al. 2011).

LOSS is an SN search that has run for over a decade monitoring nearby galaxies with a cadence of a few nights to a couple of weeks. The “full” LOSS sample contains 929 SNe, while the “optimal” LOSS sample contains 726 SNe where 98.3% of the SNe have a spectroscopic classification (Leaman et al. 2011). The LOSS detection efficiency is very high (~90%), with the vast majority of missed objects being in the nuclear regions of bright, compact galaxies (Leaman et al. 2011). The three major biases for the sample are (1) the missed objects in nuclear regions; (2) that luminous galaxies are overrepresented in the sample, an effect that increases with distance; and (3) that the Hubble type distribution changes toward earlier galaxy types with distance. However, those biases can be somewhat mitigated and do not affect certain measurements.

After constructing SN luminosity functions for each subtype, Li et al. (2011) determined that the LOSS sample is relatively complete to a distance of 80 and 60 Mpc for SNe Ia and CC SNe, respectively. Within 60 Mpc, the K-band luminosity function of the LOSS galaxy sample matches that of a complete sample for galaxies with \( M_K < -23 \) mag (Leaman et al. 2011). At fainter magnitudes, the LOSS sample is incomplete. Similarly, the average K-band luminosity for E and Scd galaxies in the LOSS sample increases by a factor of 4 and 20 from 15 to 175 Mpc, respectively (while the average galaxy increases by a factor of ~2 between 15 and 60 Mpc regardless of Hubble type; Leaman et al. 2011).

We will examine two subsamples of the LOSS sample. The “Full” sample is nearly equivalent to the “full” LOSS sample as defined by Leaman et al. (2011). We add classifications for three SNe in this sample. SN 2000cc was observed by Aldering & Conley (2000), who noted that it had a featureless spectrum consistent with a blackbody. Although that is not a definitive classification, it is consistent with a CC SN and inconsistent with an SN Ia. We also classify SN 2000ft as an SN II. Finally, Blondin et al. (2012) classified SN 2004cu as an SN Ia.

To generate the “Full” sample, we remove 24 SNe from the “full” LOSS sample. Of these 24, 6 are similar to SN 2005E (Perets et al. 2010) and 7 are SNe Iax (Foley et al. 2013). Although there is evidence that these SNe are peculiar thermonuclear SNe (e.g., Li et al. 2003; Foley et al. 2009, 2010a, 2010b, 2013; Perets et al. 2010), there is still some controversy (e.g., Valenti et al. 2009); as a result, we remove these SNe from this analysis. We also remove SN 2008J, which appears to be an SN Ia interacting with circumstellar hydrogen (Taddia et al. 2012).

After all alterations, the “Full” sample has 905 SNe, of which 368 are SNe Ia and 537 are CC SNe (137 SNe Ibc and 400 SNe II).

In Section 6, we will examine SN samples from the Sloan Digital Sky Survey (SDSS) SN survey (Frieman et al. 2008) and Palomar Transient Factory (PTF; Law et al. 2009). Both surveys are large-area untargeted surveys; the SN samples are not biased to those in luminous galaxies.

The SDSS SN survey was performed over three seasons with the SDSS telescope. Spectroscopic follow-up was performed with a variety of telescopes (Zheng et al. 2008; Konishi et al. 2011; Østman et al. 2011; Foley et al. 2012). The first cosmological results based on a spectroscopic sample were presented by Kessler et al. (2009). A photometric sample was presented by Sako et al. (2011), and a cosmological analysis of a photometric SN Ia sample was performed by Campbell et al. (2013).
PTF has been running a transient survey since 2009 using the 48 inch telescope at Palomar Observatory. Although there has not been an official spectroscopic data release yet, PTF has publicly announced several hundred spectroscopically classified SNe.

Despite being untargeted surveys, neither SDSS nor PTF is close to being spectroscopically complete. Spectroscopically complete subsamples are much smaller than LOSS. We therefore choose to focus on the LOSS sample initially and test our method with the SDSS and PTF samples.

3.2. Host-galaxy Observables

The simplest, although also the least quantitative, metric for determining bulk host-galaxy properties is the Hubble type. The Hubble types for the LOSS galaxies have been determined in a consistent way and presented by Leaman et al. (2011). Similarly, the Galaxy Zoo project has determined visual morphological classifications for a large number of SDSS galaxies (Lintott et al. 2011). They use the individual classifications of many volunteers to determine a probability that a galaxy has an elliptical or spiral morphology. The probabilities take into account biases associated with redshift.

In addition to Hubble type, one can easily measure the color of the host galaxy. Particular colors correlate well with star formation rate and should therefore correlate with the types of SNe produced. Leaman et al. (2011) present $B_r$, $B_0$, and $K$-band measurements for the LOSS galaxy sample, where $B_0$ is the $B$ magnitude corrected for Galactic extinction, internal extinction, and $K$-corrections. Since the $B$ band straddles the 4000 Å break, the $B_0 - K$ color is a reasonable proxy for the star formation rate.

Galaxy morphology is correlated with both color and luminosity. More luminous galaxies tend to be ellipticals, gas-poor, and lack recent star formation. One can generally cleanly separate star-forming and passive galaxies using a color–magnitude diagram, with both dimensions providing information. We will also examine SN populations as a function of host-galaxy luminosity. Specifically, we examine $M_K$, which is highly correlated with stellar mass.

Since CC SNe are associated with star-forming regions within a galaxy, while SNe Ia are not, we will examine the proximity of SN locations to bright regions of the host galaxy. We use the “pixel-based” method of Fruchter et al. (2006), which compares SN locations to the intensity map of a galaxy, with the brightest pixels corresponding to a value of 1 and the faintest pixels corresponding to a value of 0. We use the values provided by Kelly et al. (2008), which cover a subsample of the LOSS sample. We refer to this derived quantity as the “pixel rank.”

We also examine the offset of the SN relative to the nucleus. Both the underlying stellar population and the progenitor metallicity should correlate with the offset. For this measurement, we use the effective offset, $R$, of Sullivan et al. (2006), which is a dimensionless parameter describing the separation of the SN from its host galaxy. A value of $R = 3$ corresponds roughly to the isophotal limit of the galaxy.

4. GALAXY PROPERTIES OF THE LOSS SN SAMPLE

We now examine how host-galaxy properties can predict SN types in the LOSS sample. Figure 1 displays the fraction of SNe Ia in the LOSS sample, and the subset of SNe I, as a function of host galaxy property (morphology, color, luminosity, effective offset, and pixel ranking, respectively). Figure 1 also shows the cumulative distribution functions (CDFs) for SNe Ia, SNe II, and SNe Ibc for each host-galaxy property.

Consistently, we see that SNe Ia are more frequently found in galaxies with properties consistent with older populations than that of the CC comparison sample. Specifically, the fraction of SNe that are of Type Ia with early-type, red, or luminous host
galaxies is larger than the fraction with late-type, blue, or faint host galaxies. Therefore, the probability that a particular SN is an SN Ia is higher if its host galaxy is a luminous, red, early-type galaxy. For instance, 98% of all SNe with elliptical host galaxies are SNe Ia, while only 10% of all SNe with irregular host galaxies are SNe Ia. Clearly, host galaxy information can be useful for classifying SNe Ia with no additional information.

This trend continues even within galaxies, where SNe Ia tend to be found with larger offsets and in fainter regions of the galaxy than CC SNe. Because of the small number of LOSS SNe with pixel-ranking data, the uncertainties are especially large for that property. This metric should be re-examined when more data become available.

Figure 1 displays results for both the “Full” LOSS sample and the volume-limited LOSS sample. There are no significant differences between the samples, and most importantly, the fractions are consistent for the same bins. This indicates that whatever biases the larger LOSS sample has, they have little effect on the fraction of SNe Ia from host galaxies that are very similar in one of these properties. This result is especially important for transferring results to other surveys where galaxy population will not be the same as the LOSS survey.

5. GALSNID

Using the data above, we can create a metric for determining the probability that a given SN is of Type Ia. Specifically, this probability can be expressed using Bayes’ Theorem. Here, we consider the case where we only wish to distinguish between two choices, “Ia” and “CC.” That is, from a classification point of view, we consider all SNe to have a type, two choices, “Ia” and “CC.”

Bayes’ Theorem is

\[ P(Ia | D) = k^{-1} P(Ia) \prod_{i=1}^{n} P(D_i | Ia), \]

where \( D \) is the vector of its host-galaxy data. Since we are only considering two classes, we have

\[ 1 - P(Ia | D) = P(CC | D) \]

and

\[ 1 - P(Ia) = P(CC), \]

where \( P(T) \) is the overall probability of a given SN in the sample of Type T (the prior).

Bayes’ Theorem is

\[ P(Ia | D) = k^{-1} P(D | Ia) P(Ia), \]

where \( k^{-1} \) is a normalization factor depending on \( D \) set by requiring the class probabilities to add to unity and \( P(D | Ia) \) is the probability density of a set of observables given that the object is an SN Ia. The likelihood \( P(D | Ia) \) is difficult to model directly since \( D \) is multi-dimensional. It is convenient to neglect the correlations among the galaxy observables and make the approximation that their joint probability factors as the product of the individual one-dimensional likelihoods of each galaxy property. We can do this by invoking the Naïve Bayes assumption that the data are conditionally independent given the class, which gives us

\[ 4 \text{ This assumption is typically not true; see discussion of this limitation in Section 7.2.} \]

\[ P(Ia | D) = k^{-1} P(Ia) \prod_{i=1}^{n} P(D_i | Ia), \]

where \( D_i \) are the individual \( n \) observables.

From Equations (4), (5), and (7),

\[ k = P(Ia) \prod_{i=1}^{n} P(D_i | Ia) + (1 - P(Ia)) \prod_{i=1}^{n} P(D_i | CC). \]

The underlying population of the SNe and host galaxies is somewhat important in the determination of the probability. As an example, we consider a single observable. In that case, we have

\[ P(Ia | D) = k^{-1} P(Ia) P(D_i | Ia). \]

With some algebraic manipulation, we find that

\[ P(Ia | D) = \frac{f_{Ia/CC,x}}{1 + f_{Ia/CC,x}}, \]

where \( f_{Ia/CC,x} \) is the odds ratio of SN Ia to CC SN for a particular value of \( D_i \) (the relative fraction of SN Ia to CC SNe with \( D_i = x \)). This implies that biased samples can still be useful for determining probabilities for all other samples, both biased and unbiased, as long as the samples retain the same relative fraction of SNe Ia and CC SNe for a particular value of each observable. Specifically, the known biases of the LOSS sample should not affect our ability to apply its results to other low-redshift samples. However, using the LOSS sample for high-redshift SNe where, for example, we know that the relative fractions of SNe Ia and CC SNe are different in spirals will bias the results somewhat.

From the LOSS data, we have determined \( P(D_i | Ia) \) and \( P(D_i | CC) \) for all relevant values of each observable; this is simply the fraction of SN Ia (or CC SN) host galaxies that have a particular galaxy observable, \( D_i \). We present these data in Table 1. Since some bins do not contain many SNe, the uncertainties can be large for some values of particular parameters. To avoid potential biases associated with large statistical uncertainties, we perform a Monte Carlo simulation for each SN where we determine \( \hat{P}(D_i | T) \), a single realization of the probability for variable \( i \) using \( P(D_i | T) \) and its uncertainty. This Monte Carlo simulation is performed for all observables simultaneously, resulting in several realizations of the overall probability that a given SN is of Type Ia, \( \hat{P}(Ia | D) \). From the Monte Carlo simulation, we have a distribution of posterior probabilities that each SN is of Type Ia. We then assign the final probability, \( P(Ia | D) \), to be the median value of the distribution of \( \hat{P}(Ia | D) \).

Following the convention of psnid (photometric SN identification; Sako et al. 2011), we call this procedure galsnid (galaxy-property SN identification). For the rest of the manuscript, we define the posterior probability from galsnid as \( p \equiv P(Ia | D) \).

Having performed this procedure for the Full LOSS sample, we arrive at a distribution of probabilities from 0 to 1. We display the results in Figure 2. In this figure, we present histograms for the probability that an SN is of Type Ia for the spectroscopically confirmed subsets of SNe Ia, II, and Ibc. For the LOSS sample, 30% have \( p > 0.5 \); of those, 71% are SNe Ia. This compares favorably to the prior of \( P(Ia) = 0.41 \). For the same sample, 21% have \( p < 0.1 \), 84% of which are CC SNe.

Again, this information can be used both by itself and in combination with SN photometry for classification. We test
Table 1: Probability of Host Properties Given Type

| Bin | $P(D|\text{Ia})$ | $P(D|\text{CC})$ |
|-----|-----------------|-----------------|
|     |                 |                 |
| **Morphology** |                 |                 |
| E   | 0.141±0.001     | 0.002±0.001     |
| S0  | 0.217±0.026     | 0.017±0.007     |
| Sa  | 0.149±0.009     | 0.142±0.017     |
| Sb  | 0.177±0.023     | 0.188±0.020     |
| Sbc | 0.117±0.009     | 0.231±0.022     |
| Sc  | 0.120±0.017     | 0.218±0.021     |
| Scd | 0.076±0.013     | 0.188±0.018     |
| Irr | 0.003±0.004     | 0.015±0.006     |
| $B_0 - K$ |                 |                 |
| 0.0–1.75 | 0.026±0.000 | 0.044±0.010 |
| 1.75–2.25 | 0.023±0.000 | 0.075±0.013 |
| 2.25–2.5 | 0.037±0.009 | 0.068±0.013 |
| 2.5–2.75 | 0.043±0.010 | 0.115±0.016 |
| 2.75–3.0 | 0.111±0.009 | 0.181±0.018 |
| 3.0–3.25 | 0.131±0.011 | 0.185±0.020 |
| 3.25–3.5 | 0.154±0.022 | 0.197±0.026 |
| 3.5–3.75 | 0.125±0.020 | 0.115±0.014 |
| 3.75–4.0 | 0.168±0.023 | 0.048±0.011 |
| 4.0–4.25 | 0.103±0.014 | 0.022±0.008 |
| 4.25–6.25 | 0.080±0.007 | 0.010±0.004 |

Effective Offset

| 0.0–0.05 | 0.043±0.002 |
| 0.05–0.1 | 0.098±0.018 |
| 0.10–0.15 | 0.130±0.020 |
| 0.15–0.2 | 0.090±0.014 |
| 0.20–0.25 | 0.071±0.005 |
| 0.25–0.3 | 0.057±0.014 |
| 0.30–0.35 | 0.068±0.015 |
| 0.35–0.4 | 0.060±0.014 |
| 0.40–0.45 | 0.038±0.009 |
| 0.45–0.5 | 0.052±0.013 |
| 0.50–0.55 | 0.060±0.014 |
| 0.55–0.6 | 0.060±0.014 |
| 0.60–0.65 | 0.062±0.014 |
| 0.65–0.7 | 0.062±0.014 |
| 0.70–0.75 | 0.073±0.013 |
| 0.75–0.8 | 0.073±0.013 |
| 0.80–0.85 | 0.064±0.010 |
| 0.85–0.9 | 0.052±0.013 |
| 0.90–0.95 | 0.046±0.013 |

Pixel Rank

| 0.0–0.2 | 0.206±0.094 |
| 0.2–0.4 | 0.294±0.109 |
| 0.4–0.6 | 0.088±0.068 |
| 0.6–0.8 | 0.324±0.113 |
| 0.8–1.0 | 0.088±0.068 |

Figure 2. Histogram of $galsnid$ probability for different spectroscopic SN classes in the LOSS sample. The filled black, red, and blue histograms represent SNe Ia, Ibc, and II, respectively.

(A color version of this figure is available in the online journal.)

Figure 3. Efficiency, purity, and FoM (blue, red, and black curves, respectively) for subsamples of the LOSS sample defined by a particular $galsnid$ probability or larger. The FoM peaks at $p = 0.97$ at a value that is 2.23 times larger than the FoM for the entire sample.

(A color version of this figure is available in the online journal.)

the utility of using only the $galsnid$ method with the FoM defined in Section 2. Figure 3 presents the efficiency, the purity ($W_{\text{p}} = 1$), and the FoM (assuming $W_{\text{p}} = 5$) for subsamples including only objects with $galsnid$ probability $p$ greater than a threshold value. The FoM peaks at $p = 0.97$ at a value of 0.269. The full sample has an FoM of 0.121, so implementing $galsnid$ improves the FoM by a factor of 2.23. As a comparison, Campbell et al. (2013) performed $psnid$ on a simulated sample of SNe Ia and obtained an improvement of 2.60.

6. TESTS

In this section, we perform a variety of tests on the $galsnid$ method for classifying SNe. Specifically, we examine the reliability of the method, test the importance of each galaxy observable for classification, and apply the method to additional SN samples.
Having shown that host-galaxy information is useful for SN classification, we now test the robustness of the above results. Specifically, we cross-validate the method again using the LOSS sample. We split the sample in half, placing every other SN (to mitigate possible biases in the SN search or classification with time) as the training and comparison samples. Using the “evenly indexed” sample as the training set, we find the galsnid probability that results in the highest FoM for the training set, which we consider the threshold value above which an SN will enter our final sample. We then determine the efficiency and pseudo-purity of the sample. Doing this, we find that the FoM improves by a factor of 1.4 compared to not using the galsnid procedure. Performing the same procedure but switching the training and testing samples, we find that the FoM improves by a factor of 2.4. Therefore, the method appears to be robust within a given sample, although clearly the amount of improvement depends on the training sample.

6.2. Importance of Each Observable

To assess the importance of each host-galaxy observable for classification, we first re-analyze the data and compute galsnid probabilities using a single observable at a time. We then compute the galsnid probabilities using all observables, but excluding a single observable at a time. The summary of the results is presented in Table 2, where we list the peak FoM, the improvement factor over the baseline FoM, and the difference in the median galsnid probability for the spectroscopically confirmed SNe Ia and CC SNe classes. The latter is a measure of the difference in distribution of galsnid probabilities for different spectroscopic classes, and thus an additional (and different) indication of the importance of the observable beyond the improvement in the FoM.

Unsurprisingly, the pixel ranking data were not particularly useful, and excluding them made no significant difference in the results. The vast majority of SNe in the sample do not have pixel ranking data, and thus it only has the ability to affect a small number of objects. Additionally, pixel ranking does not appear to be as discriminating as other observables.

The color and luminosity are both somewhat important. The median galsnid probability when just using color (luminosity) was 0.43 (0.47) and 0.33 (0.40) for SNe Ia and CC SNe, respectively. However, just using color or luminosity results in only a modest improvement in the peak FoM, with ratios of 1.06 and 1.12, respectively. Using both quantities together (but excluding all other observables) results in a maximum FoM improvement ratio of 1.17.

Removing either color or luminosity results in only modest changes in the maximum FoM from 0.269 to 0.273 (a net increase). We do not consider this change in the FoM significant. However, removing these data results in more smearing of the populations with the difference in the median galsnid probabilities for SNe Ia and CC SNe decreasing from 0.34 to 0.26 and 0.24, respectively. Removing both color and luminosity continues this trend, with a difference in medians for the two populations of only 0.16. Therefore, although color and luminosity do not significantly affect the peak FoM presented here, they could be particularly important for other applications or different FoMs.

Using only offset information results in no significant improvement in maximum FoM, although it is slightly helpful with classification; the median galsnid values for the SN Ia and CC populations are 0.44 and 0.41, respectively. However, removing the relative offset decreases the maximum FoM to 0.261. This is a somewhat surprising result and may not be significant.

By far, the most important parameter is morphology. Morphology alone results in a maximum FoM of 0.262, a factor of 2.18 improvement over not using any host-galaxy information. Removing morphology information decreases the maximum FoM to 0.157. Without these data, the maximum improvement is only a factor of 1.30 over not using any host-galaxy data. Nonetheless, galsnid is still effective without morphology.

6.3. SDSS

We also examined the largest photometry-selected SN Ia sample: the SDSS-II SN survey compilation (Sako et al. 2011; Campbell et al. 2013). This sample, which we call the “SDSS sample,” was taken from the SDSS-II SN survey, and various cuts were made based on the photometric properties of the SNe to determine a relatively pure subsample of SNe Ia (see Campbell et al. 2013 for details). This sample is a subset of the full photometric-only sample of SNe from SDSS-II (Sako et al. 2011). All SNe in the SDSS sample have host-galaxy redshifts.

Using simulations, Campbell et al. (2013) showed that the SDSS sample should have an efficiency of 71% and a

| Observable          | Exclusively Using Observable | Excluding Observable |
|---------------------|------------------------------|----------------------|
|                     | Peak FoM Improvement Factor | Difference in Medians|
|                     |                              |                      |
| Baseline            | 0.121                        | N/A                  | 0.121 N/A N/A        |
| Using all galaxy    | 0.269 2.23                  | 0.34                 | 0.269 2.23 0.34      |
| Morphology          | 0.262 2.18                   | 0.15                 | 0.157 1.30 0.22      |
| Color               | 0.128 1.06                   | 0.10                 | 0.273 2.26 0.26      |
| Luminosity          | 0.135 1.12                   | 0.07                 | 0.273 2.27 0.24      |
| Effective offset    | 0.122 1.02                   | 0.03                 | 0.261 2.16 0.30      |
| Pixel rank          | 0.123 1.02                   | 0.00                 | 0.269 2.23 0.33      |

Notes.

a The “Baseline” category classifies the entire SN sample as SN Ia without using host-galaxy information.
b This category is for the nominal galsnid procedure, as defined in Section 5, using all host-galaxy data.
contamination of 4%. This sample only includes SNe photometrically classified as Type Ia.

Using the SDSS imaging data of the host galaxies, we apply the $galsnid$ procedure to the SDSS sample. This sample is already supposedly quite pure, and an ideal method would provide a criterion to sift out the 4% contamination without a large loss of true SNe Ia. Of course, this is not a perfect test of a given method since increased efficiency with minimal decrease in purity is also a net gain. Nonetheless, a qualitative assessment can be made.

For this test, we focused on the SNe with $z < 0.2$. This subsample is likely to have some contamination from CC SNe; Malmquist bias will remove many low-luminosity CC SNe from the higher-redshift sample. The efficiency for this subsample is also expected to be higher, providing a more representative SN Ia sample. For these redshifts, one may also expect that the fractions of different SN types for a given galaxy property have not evolved much. For the SDSS sample, the SN parameters (light-curve shape and color) do not evolve much for this redshift range. Additionally, a significant number of SNe in this sample are spectroscopically confirmed as SNe Ia. Finally, Campbell et al. (2013) show that simulations predict several large Hubble-diagram outliers from CC SNe at $z < 0.2$ that remain in the sample. Although there is no direct evidence of that contamination, there are also several Hubble-diagram outliers at $z < 0.2$ in the data as well. Understanding this potential contamination and potentially identifying a solution would be useful. This subsample contains 143 SNe, but only 131 have matches for the listed galaxy ID in DR8/9 (Ahn et al. 2012; Aihara et al. 2011). We require host-galaxy photometry and a host-galaxy redshift for this analysis.

The overall fraction of SNe Ia in the Full and volume-limited LOSS sample is 40% and 27%, respectively. Bazin et al. (2009) found that only 18% of SNe at $z < 0.4$ in the Supernova Legacy Survey were SNe Ia. However, using the volumetric rates as a function of redshift from Dilday et al. (2008) and Bazin et al. (2009; for SNe Ia and CC SNe, respectively), we find that the SN Ia fraction should be 22% at $z = 0.15$. Of course, this is the volumetric fraction. SDSS is relatively complete to $z = 0.2$, but still suffers from some Malmquist bias. The magnitude-limited SN Ia fraction in the LOSS sample was 79% (Li et al. 2011). For the SDSS sample, we take an intermediate value of 50%. This number essentially provides a normalization for the probability and does not affect relative results.

Taking the DR8 imaging data, we determined the $ugriz$ magnitudes for each host galaxy. Cross-checking with earlier data releases, we verified that no measurements were significantly affected by SN light. Using the $kcorrect$ routine (version 4.1.4; Blanton et al. 2003; Blanton & Roweis 2007), we calculated rest-frame $B$ and $K$ magnitudes. This method extrapolates galaxy templates into the near-IR to estimate the $K$ magnitudes, but since these galaxies have five-band photometry, including $z$ band, this extrapolation should be relatively robust. We tested this by comparing the observer-frame $z$ and extrapolated observer-frame $K$ photometry; the two values were highly correlated. From the derived photometry, we were able to measure $B - K$ and $M_K$ for each SDSS host galaxy.

We also used morphological classifications from the Galaxy Zoo survey (Lintott et al. 2011). Only 33 of the 131 SN host galaxies have morphological classifications from Galaxy Zoo. Using the LOSS data, we re-determined the probabilities of an SN being of Type Ia when only using the coarse bins of “elliptical” and “spiral.” These probabilities are used for the SDSS galaxies with morphology information.

Since the effective offset and pixel ranking are not particularly effective at classifying SNe, we do not use those measurements.

For comparison, we also chose 10,000 random galaxies in the SDSS-II SN survey footprint with $z < 0.2$. We expect that these galaxies will have average properties that are different from both the average SN Ia host galaxy and the average SN host galaxy. As a result, performing the $galsnid$ procedure on these galaxies should provide a baseline for any potential improvement.

The $galsnid$ probabilities are shown for these two samples in Figure 4. We find that the median $galsnid$ probabilities for the SDSS sample and the random comparison sample are 0.82 and 0.66, respectively. The SDSS host-galaxy sample is more likely to host SNe Ia (relative to CC SNe) than the random sample. This is further validation of the $galsnid$ procedure. However, the probabilities are more evenly distributed than for the LOSS sample. We attribute this mainly to the lack of morphology information for the majority of the sample.

We examined SDSS images for each host galaxy in the SDSS sample, and one of us (R.J.F.) visually classified their morphology as elliptical or spiral. We were able to assign a morphology to 87 of the 131 galaxies, of which 36 and 51 were elliptical and spirals, respectively. These classifications are not as robust as the Galaxy Zoo measurements, but are helpful for assessing how morphology data can improve our classifications.

After including these new morphology measurements (and ignoring all Galaxy Zoo measurements), we find that the median $galsnid$ probability of the SDSS sample is 0.85, slightly above the median of the previous analysis. Moreover, the number of SNe with $p > 0.97$, the peak of the FoM from the prior analysis, more than tripled from 11 to 36 SNe. Using the best-fit cosmology of Campbell et al. (2013), we are also able to measure the Hubble residual for each SN in the sample. Notably, there are six (nine) SNe with a Hubble residual $>0.5$ (0.4) mag from zero. Figure 5 displays the absolute value of the Hubble residual as a function of $galsnid$ probability. Interestingly, three of these SNe, including the most discrepant outlier, have $p < 0.2$. There are only 18 SDSS SNe with $p < 0.2$, and thus the outliers make up 17% of the low-probability subset.
Splitting the SDSS sample by $p = 0.85$ (the median value), we can examine the characteristics of SNe with low/high galsnid probability. The average and median redshifts for the two samples are nearly identical, with the high-probability subsample being at slightly higher redshift (by 0.01).

Looking at the subsamples in detail, we see a correlation between Hubble residual (not the absolute value) and galsnid probability. SNe with large galsnid probability tend to have negative Hubble residuals, while those with small galsnid probability tend to have positive Hubble residuals.

We display these residuals in Figure 6. The medians for these subsamples are $-0.138$ and $0.041$ mag, respectively. The weighted means are $-0.085 \pm 0.011$ and $0.034 \pm 0.012$. The difference in the weighted means is $7.3\sigma$. Performing a Kolmogorov–Smirnov test on the two samples results in a $p$-value of $4.4 \times 10^{-6}$, indicating that the Hubble residuals are drawn from different populations.

Considering that most of the SNe in the $z < 0.2$ subsample are spectroscopically confirmed as Type Ia, the difference in Hubble residuals is probably not the result of contamination. Rather, the difference is likely related to the known correlation between Hubble residuals and host-galaxy properties (Kelly et al. 2010; Lampeitl et al. 2010; Sullivan et al. 2010). Campbell et al. (2013) chose not to include this correction. Since galsnid probability correlates strongly with these host-galaxy properties, this is likely the cause of the difference in Hubble residuals. However, not accounting for this effect prevents some analysis of the correlations between Hubble residuals and galsnid probability.

Excluding the outlier SNe (Hubble residuals $>0.5$ mag), we fit Gaussians to the residuals. Splitting the sample by $p = 0.85$, we find that the standard deviations of the residuals are $0.128$ and $0.114$ mag for the subsample with $p \leq 0.85$ and $p > 0.85$, respectively; the subsample with higher galsnid probability has smaller scatter. It is unclear whether the difference is the result of different amounts of contamination in the subsamples or because the properties of SNe Ia in redder, more luminous, earlier galaxies tend to produce a more standard sample.

The host galaxies of the six outlier SNe (Hubble residual $>0.5$ mag) are somewhat varied: two large spiral galaxies, an incredibly small and low-luminosity galaxy, a modest disk galaxy, a small red galaxy with no signs of star formation, and a small starburst galaxy with a potential tidal tail. There is no obvious trend with the host-galaxy properties investigated here. Nonetheless, galsnid provides some handle on these outliers.

### 6.4. PTF

To further test the galsnid method on another independent sample, we investigate the relatively large sample of publicly classified SNe from PTF. PTF is a low-redshift (typically $z < 0.15$) SN survey that has spectroscopically classified almost 2000 SNe (as of 2013 June 1). Many of these SNe are publicly announced with coordinates, redshifts, and classifications. PTF provides a relatively large sample of SNe for which we can attempt classification through host-galaxy properties.

Using the WISEREP database (Yaron & Gal-Yam 2012), we obtained a list of 555 PTF SNe with classifications. We visually cross-referenced this list with SDSS images to determine the host galaxy for each SN. Many SNe were not in the SDSS footprint, had no obvious host galaxy, or there was some ambiguity as to which galaxy was the host. After removing these objects, 384 SNe remained. We further restricted the sample to SNe with host galaxies that have SDSS spectroscopy, leaving a total of 151 SNe. This sample contains 118 SNe Ia and 33 CC SNe. We again match the Galaxy Zoo morphology classifications to this sample. For the PTF sample, 131 host galaxies had classifications.

Using the same method as described in Section 6.3, except using the LOSS prior on the SN Ia fraction, we applied the galsnid technique to the PTF sample. Histograms of the resulting probabilities are presented in Figure 7. Again, the SNe Ia typically have a much higher galsnid probability than the CC SNe. The median probabilities for the SNe Ia and CC SNe are 0.74 and 0.27, respectively. This is empirical proof that simply using the LOSS parameters is useful for classifying SNe in an untargeted survey.

### 7. DISCUSSION

#### 7.1. Additional Applications

Although we have focused on separating SNe Ia from CC SNe, the galsnid algorithm can be used for a variety of purposes. As an example, we have used the galsnid algorithm to separate SNe Ibc from SNe II in the LOSS sample (Figure 8). Although the two samples do not separate as cleanly as SNe Ia from CC
SNe, one can use \textit{galsnid} to prioritize SNe for follow-up. The method can be particularly useful when an SN is young, before any light-curve fitting can be performed.

Similarly, we can even separate different subclasses of SNe. As an example, \textit{galsnid} was used to separate “peculiar” SNe II from “normal” SNe II (Figure 9). Specifically, we were able to separate SNe classified as SNe Iib or SNe IIn from those classified as SNe IIP or simply SNe II. Again, \textit{galsnid} is useful for selecting SNe for follow-up. In this case, it could be particularly useful since early spectra of all types of SNe II can be relatively featureless, and thus there could be epochs where the host-galaxy information is more discriminating than a spectrum.

Another potential application is classifying the small number of unclassified SNe in the LOSS sample. For these SNe, we applied the \textit{galsnid} procedure using the LOSS priors and probabilities. Since these SNe were part of the LOSS sample, it is reasonable to assume that the absolute probabilities are correct. That is, an SN with \( p > 0.5 \) is likely an SN Ia. We list the results in Table 3.

Of the 10 unclassified SNe, 8 are classified as CC (although SN 2006A, with \( p = 0.497 \), is effectively undetermined). Interestingly, SN 2006dz, which \textit{galsnid} classifies as an SN Ia, was originally identified in template-subtracted images of another SN, SN 2006br (Contreras & Folatelli 2006). The SN was identified after maximum brightness, and the SN appears to be heavily dust reddened. Nonetheless, the light curves are consistent with being an SN Ia.

Summing the \textit{galsnid} \( p \) values for the SNe classified as CC and \( 1 - p \) for those classified as SNe Ia, we can estimate the number of incorrectly classified SNe in this sample. For the spectroscopically unclassified LOSS sample, we expect incorrect classifications for 2.055 SNe out of 10 SNe.

### 7.2. Further Improvements to Galsnid

The current \textit{galsnid} method is presented mainly as a proof of concept. There are several improvements one should make before using \textit{galsnid} for specific robust scientific results.

The current methodology of \textit{galsnid} presumes that all host-galaxy properties are uncorrelated. This is clearly incorrect. As a result, we have some information about other parameters with a single measurement. Specifically, color, luminosity,
and morphology are correlated. Taking these correlations into account should improve our inference.

There are a number of additional parameters that one could measure for a host galaxy. For the LOSS sample, we simply use morphology, a single color, a single luminosity, an effective offset, and a pixel ranking. Adding additional photometry in several bands should improve classification. Deriving physical quantities such as star formation rates and masses from such data may also provide more robust classifications.

Adding data from spectroscopy should also improve classification. Specifically, emission-line luminosity (to measure star formation rates; e.g., Meyers et al. 2012), line diagnostics (to determine possible active galactic nucleus contribution to photometry), velocity dispersion (to measure a mass), and metallicity could all be important discriminants. Additional data such as H I measurements could be useful, but perhaps difficult to obtain for large samples.

One could also possibly include other environmental information in a classifier. The density of the galactic environment may affect the relative rates of SNe. Perhaps close companions are a good indication of a recent interaction that triggered a burst of star formation.

Future investigations should attempt to provide a broader set of observations from which classifications can be made.

### 7.3. Combining Classifications

Using host-galaxy properties to classify SNe has several distinct advantages over light-curve analyses. It does not use any light-curve information, so samples will not be biased based on expectation of light-curve behavior. Almost all host-galaxy data can be obtained after the SN has faded. In particular, high-resolution imaging, spectroscopy, or additional photometry can be obtained post facto.

Since galsnid is independent from any light-curve classifier, one can use SN Ia samples defined by both techniques to examine systematics introduced by either method.

Host-galaxy data can also be combined with photometry-only classification, and one can implement hybrid approaches. Since galsnid produces a probability density function for each SN, it would be trivial to naively combine the output of galsnid with any other similar output. However, some SN properties are correlated with host-galaxy properties. For instance, SNe Ibc tend to come from brighter galactic positions than SNe II, and SNe Ia hosted in ellipticals tend to be lower luminosity than those hosted in spirals. Therefore, a more careful approach to combining different methods should be used.

In addition to classifications made purely on host-galaxy or light-curve properties, one could use hybrid measurements. For instance, the peak luminosity of an SN compared to the luminosity of its host galaxy or the relative colors of an SN and its host galaxy could be useful indicators.

### 7.4. Redshift Evolution

The relative fraction of SN classes changes with redshift, with the SN Ia fraction decreasing with redshift to at least \( z \approx 1 \). Similarly, galaxy properties change, on average, over redshift ranges of interest. It is not known if the fractions over a small parameter range change. For instance, it is reasonable to assume that the SN Ia fraction in ellipticals has relatively little evolution. The fractions in other small bins might also stay the same while the underlying galaxy population is changing with redshift.

The assumption that there is little evolution in the relative fractions for small parameter ranges should be tested with data. However, even with this assumption, one needs to account for the overall evolution of the galaxy population for high-redshift samples. A simple approach is to have a prior for the overall (observed) fraction as a function of redshift. Such a prior can be determined both observationally and through simulations.

However, if one uses a threshold of a particular galsnid probability to separate classes, the effect of the prior is minimized. That is, the classification of a particular SN is only affected if the different prior would cause the galsnid probability of that object to cross the threshold. For example, if there are objects with \( p = 0.99, 0.95, 0.9, 0.8, \) and 0.6 with \( P( \text{Ia} ) = 0.5 \), changing the prior to \( P( \text{Ia} ) = 0.4 \) will result in probabilities of approximately 0.985, 0.93, 0.86, 0.73, and 0.5, respectively. If the threshold were \( p = 0.94 \), only one of the example SNe would have had their classification changed with the different priors. This example also demonstrates that objects with \( p \approx 0.5 \) are more affected by the prior than those close to zero or one.

### 7.5. When Not to Use galsnid

The galsnid method can produce relatively clean samples of particular SN classes. However, these samples can be highly biased subsamples of the underlying SN class. For instance, when choosing an SN Ia sample, SNe with elliptical hosts will be much more likely to be included than those in spirals. But since SN Ia properties such as luminosity are correlated with host-galaxy properties (e.g., Hicken et al. 2009), a galsnid-defined sample will likely be biased to lower-luminosity SNe. Similar biases are also introduced by light-curve classifiers (SN Ia with light curves more like the templates and less like CC SNe are more likely to be included); however, the galsnid biases may be harder to properly model. Similarly, as seen in Section 6.3, cosmological analyses could be biased if correlations between host-galaxy properties and Hubble residuals are not removed. Again, these biases also apply to light-curve classifiers that are more likely to select SNe with particular light-curve properties as SNe Ia and if those properties (e.g., color) correlate with Hubble residuals (Scollnic et al. 2013).

As a result, one must be careful in choosing appropriate applications for galsnid samples. Clearly, investigations of host properties of a given class should not be performed on a galsnid sample. If one were to use a galsnid sample to determine SN rates as a function of redshift, careful attention to the prior is required. Additionally, SNe with particularly large offsets could have misidentified host galaxies. Although this should not affect many SNe, galsnid may not provide representative samples specifically designed to identify such objects.

### 8. CONCLUSIONS

We have introduced a method for classifying SNe using only galaxy data. This method relies on the fact that different SN classes come from different stellar populations. Using the LOSS sample, we estimate the probabilities that particular SN classes have specific host-galaxy properties and the probabilities that galaxies with particular properties have particular SN classes. We define an algorithm, galsnid, that combines the host-galaxy data to determine the Bayesian posterior probability that a given SN is of a particular class.

We have tested galsnid in a variety of ways and have determined that it provides robust, reliable classifications under many different scenarios. We find that of the quantities examined
here, morphology had the most discriminating power. We have shown that \textit{galsnid} is effective at building relatively pure samples of particular SN classes and can be helpful for building samples for SN Ia cosmology. We also demonstrated some additional applications for \textit{galsnid}, including separating various subclasses.

Past (SDSS), current (Pan-STARRS; PTF), and future SN surveys (Dark Energy Survey; the Large Synoptic Survey Telescope) should have deep imaging of all SN host galaxies as a result of the nominal survey. These data could be used for classification with \textit{galsnid} without additional observations. However, a relatively small spectroscopic campaign could provide detailed information that should improve classifications beyond those presented here. Moreover, high-resolution adaptive-optics or \textit{Hubble Space Telescope} imaging could significantly improve any classification by allowing a precise morphological classification.

Additional improvements to \textit{galsnid} could be achieved by taking into account additional galaxy data, properly handling correlated data, joining galaxy and SN data, and combining \textit{galsnid} results with those of photometry-based SN classifiers.

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