Novel adsorption model of filtration process in polycarbonate track-etched membrane: Comparative study

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Abstract

Current assumptions are used in the formulation of pseudo-first (PFO) and second-order (PSO) models to describe the kinetic data of filtration based on ideal operating conditions. This paper presents a new model developed with pseudo \( n \)th order and based on real assumption. A comparison was performed between PFO, PSO and the new model to highlight their performance and the optimisation of the pseudo-order equation, using MATLAB software. Adsorption characteristic of bovine serum albumin adsorption on the track-etched membrane are used as a medium based on protein filtration data were extracted from the literature for different concentrations to demonstrate the comparison between PFO/PSO and the new model. The pseudo first and second-order kinetic models were applied to test the experimental data and they did not provide reasonable values. The results show that the predicted values are consistent with experimental values giving a good correlation coefficient \( R^2 = 0.997 \) and a minimum root mean squared error RMSE = 0.0171. Indeed, the experimental results follow the new model and the optimal pseudo equation order \( n = 1.115 \), the most suitable curves for the new model. As a result, we used different experimental adsorption data from the literature to examine and check the applicability and validity of the model.

Keywords: Adsorption, Bovine serum albumin, Membrane filtration, Modelling

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1. Introduction

The development of membrane technology has been considerably expanded in many areas, particularly in food industry, water reuse and effluent treatment. Membrane fouling by protein is an inevitable phenomenon and one of the real obstacles which reduce the performance of the filtration process. Consequently, the control and the anticipation of fouling are required for the proper management of the operation.

According to Karros et al. [1], membrane fouling is a complex phenomenon that can be irreversible with solute adsorption, which is characterised by the blocking of membrane pores during filtration by the combination retention, accumulation, and adsorption of particles and compounds on the membrane or in the membrane’s pores. This phenomenon is the basis of a physical, chemical and biological nature, which leads to a decrease of both permeability and a variation in selectivity [2, 3].

In recent years, the adsorption property of microfiltration membrane proteins is used as an indicator of membrane performance [4]. The kinetic development of adsorption requires a knowledge and understanding of the complexity of its mechanisms. Several models have been developed to predict the expression rate of the adsorption mechanisms [5]. Most research in this field report experimental results about the adsorption capacity of solutes at equilibrium and about the kinetics of adsorption. The data are then described using various models or empirical formulas.

In the literature, two types of equations have been commonly used to represent the kinetics. Pseudo-first-order (PFO) and pseudo-second-order (PSO) models are the two most adopted empirical models in liquid adsorption studies [6].

Pseudo first-order kinetic was initially proposed at the end of the 19th century by Lagergren [7]. PSO kinetic was introduced in the middle of the 80’s [8, 9].

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Later, Ho [10] showed that PSO equation could be presented in four linear forms with a very different least squares regression analysis, thus different obtained constants. However, Ho concluded that the best fit kinetic parameters should be obtained using a nonlinear method. Following Ho's work, other researchers [11, 12] have shown that it is practical to predict adsorption kinetics as well as the best linearization technique for the most suitable kinetic model. Though, it is not an appropriate fit kinetic method.

However, the nonlinear technique curve fitting of PSO and PFO equations needs to be solved by trial and error [10], while it will be an appropriate method in the prediction of the adsorption kinetic.

Furthermore, in addition to a first and second precise pseudo-order (PFO and PSO), a new approach has been developed based on the diffusion equation, which has proven to be an excellent quantitative prediction agreement [13]. Simonin [14] also examined a comparison of pseudo- first-order and PSO rate laws for the description of liquid/solid adsorption kinetics where the pseudo- second-order reaction kinetics provides the best correlation of experimental data.

More recently, four research studies have shown that an error in the use of a pseudo-first-order kinetic model requires correction [15-18]. Moreover, Tseng and Wu [19] proposed a convenient method to determine kinetic parameters of adsorption processes by nonlinear regression of the PFO, PSO and pseudo-nth-order (PNO) equations with SigmaPlot 11 software. They have provided the best fit kinetic parameters of PNO equations which allow describing the adsorption process better than using traditional equation (PFO/PSO). Of these articles, some demonstrated that the PSO equation suitably fitted their experimental data, and some further showed that PSO equation is more reasonable than PFO equation.

Recently, many studies based on the adsorption of bovine serum albumin (BSA) on a
porous polyethylene membrane, have been proposed as an improvement of a simple physical model [20]. The PSO kinetic model is the most favoured, applicable and relevant kinetic model compared to the first-order pseudo kinetic model for the adsorption behaviour of BSA [21-23]. As a result it is difficult to correlate adsorption data with variables by simple mathematical modelling. Therefore, an artificial neural network (ANN) offers an advantageous tool [24, 25].

Fu and Xu [26] have improved an artificial back-propagation neural network (BP-ANN) successfully used to model the adsorption of BSA on a porous polyethylene membrane. This paper presents a new model to determine the kinetic parameters of the non-linear regression adsorption process. However, a non-linear regression of the pseudo- first-order, pseudo- second-order and model equation was performed and an optimisation of the pseudo-order n was performed using the MATLAB software. In addition, adsorption characteristic curves were plotted to highlight the differences between the PFO, PSO and the new model equations. This model is used to describe the parameters of adsorption correlation of BSA solution using polycarbonate track-etched (PCTE) membrane media. These kinetic data were provided to investigate the applicability and validity of the proposed model. Minimum root mean square error and least linear - squares($R^2$) were used to indicate the most appropriate order.

The utility of the model is not limited to the prediction of the experimental data chosen for model validation. In addition, its predictive capacity and the validity of the proposal should also allow the model parameters for other experiments and measurements to be studied and estimated from correlations.
2. Methodology

2.1. Kinetic Study

In order to investigate and demonstrate the absorption of BSA solution using PCTE membrane media, a new model has been established to predict the adsorption kinetic process. In addition, a comparative study was carried out with the Pseudo First and Second Order equations using the experimental data reported by Ho and Zydney. Ho and Zydney [27] conducted an experiment of measurement and test samples of suspensions with different concentrations ranging from 0.5 to 5g/L, under different pressures. Experimental data has been summarised in Table 1.

Table 1. Experimental Conditions Reported by Ho and Zydney [27].

| Media Membrane | GE polycarbonate track etched membrane |
|----------------|----------------------------------------|
| Pore diameter  | 0.2μm                                  |
| Normal thickness | 10μm                              |
| Porosity       | 0.14                                  |
| BSA solutions  |                                        |
| Suspensions    | Concentration 0.5, 1.0, 1.4, 2.0, 5.0 g/L |
| Operating pressure | 0.8, 2.0, 4.0, 8.0 Psi |

As a result, the ability of the proposed model to describe the experimental kinetic data was evaluated by adjusting this rate law to the experimental data. In addition, the values were obtained by digitalising the item numbers using Getdata. Graph. Digitizer 2.24 software. The results summarised in Table 2 are presented in Fig. 1.

Table 2. Experimental Data Extracted with Getdata. Graph. Digitizer software [28].
| C=0.5gL⁻¹ | C=1.0gL⁻¹ | C=1.4gL⁻¹ | C=2.0gL⁻¹ | C=5.0gL⁻¹ |
|-----------|-----------|-----------|-----------|-----------|
| t (sec)   | v (m²m⁻²) | t (sec)   | v (m²m⁻²) | t (sec)   | v (m²m⁻²) | t (sec)   | v (m²m⁻²) | t (sec)   | v (m²m⁻²) |
| 0         | 0         | 0         | 0         | 0         | 0         | 0         | 0         | 0         | 0         |
| 0         | 0         | 0         | 0         | 0         | 0         | 0         | 0         | 0         | 0         |
| 250.87    | 0.208     | 433.90    | 0.315     | 176.99    | 0.077     | 103.56    | 0.0737    | 193.55    | 0.080     |
| 473.87    | 0.358     | 596.61    | 0.417     | 309.73    | 0.142     | 233.01    | 0.142     | 354.84    | 0.142     |
| 752.61    | 0.497     | 1,274.58  | 0.648     | 420.35    | 0.22      | 284.79    | 0.204     | 612.90    | 0.154     |
| 891.98    | 0.601     | 1,545.76  | 0.694     | 530.97    | 0.279     | 414.24    | 0.233     | 1,096.77  | 0.185     |
| 1,226.48  | 0.694     | 1,979.66  | 0.731     | 575.22    | 0.320     | 543.69    | 0.289     | 1,612.90  | 0.216     |
| 1,393.73  | 0.775     | 2,277.97  | 0.768     | 840.71    | 0.362     | 724.92    | 0.312     | 2,225.81  | 0.222     |
| 1,672.47  | 0.844     | 2,766.10  | 0.805     | 1,150.44  | 0.433     | 906.15    | 0.335     | 2,709.68  | 0.25      |
| 2,090.59  | 0.936     | 3,118.64  | 0.805     | 1,371.68  | 0.469     | 1,190.94  | 0.357     | 3,193.55  | 0.272     |
| 2,397.21  | 0.983     | 3,742.37  | 0.87      | 1,792.04  | 0.510     | 1,501.62  | 0.392     | 3,774.19  | 0.296     |
| 2,815.33  | 1.041     | 4,149.15  | 0.796     | 2,101.77  | 0.569     | 1,786.41  | 0.42      | 4,516.13  | 0.306     |
| 3,623.69  | 1.098     | 4,691.52  | 0.944     | 2,389.38  | 0.575     | 2,433.66  | 0.459     | 5,129.03  | 0.327     |
| 4,348.43  | 1.179     | 5,423.73  | 0.9722    | 2,699.12  | 0.605     | 3,003.24  | 0.494     | 5,709.68  | 0.333     |
| 5,128.92  | 1.237     | 3,008.85  | 0.629     | 4,220.06  | 0.505     |            |            |            |            |
| 6,020.91  | 1.283     | 3,318.58  | 0.629     | 6,006.47  | 0.562     |            |            |            |            |
|           |           | 3,606.19  | 0.647     |           |           |            |            |            |            |
Fig. 1. Plot of filtrate volume $V$ vs time $t$ for five experiments $c = 0.5 \text{g/L}, c = 1.0 \text{g/L}, c = 1.4 \text{g/L}, c = 2.0 \text{g/L} \text{ and } c = 5.0 \text{g/L}$.

2.1.1. Adsorption kinetics modelling

A number of studies based on the pseudo and physical laws of filtration (Langmuir, Freundlich, pseudo first and second-order) exist in the literature giving incorrect results based on a hypothesis, although this hypothesis used in the formulation of filtration laws is incorrect. To overcome these errors, a new model has been proposed with pseudo $n^{th}$ order using a true hypothesis based on real conditions:

- Solid surface is not uniform;
- Adsorption heat depends on the recovery rate of the solid surface;
- Adsorption is done using two layers;
- No balance exists between the molecules of the two phases;
- Filtration can be addressed by adsorption;
- Morphological meshes of the membrane structure are equivalent to the sites;
- Fouling begins after filling the meshes;
Physico-chemical parameters are independent of temperature and initial concentration; According to filtration variation rate over time, it is assumed that the chemical substances present in the feed can be absorbed by the membrane and/or the cake layer and the adsorption rate can be defined by the expression pseudo $n^{th}$ order kinetic:

$$\frac{dq}{dt} = k_n(q_{max} - q_t)^n \quad (1)$$

Where, $n$ is the real number ($n \in R^+$), $q(t)$ is the adsorbed amount of protein per unit of membrane mass $(mg/g)$, $q_{max}$ is the maximum adsorption capacity of the membrane $(mg/g)$ and $k_n$ the constant of the reaction rate $[(mg/g)^{1-n}s^{-1}]$.

It is assumed that the removal of adsorbed substances is incomplete by an overall balance of the adsorbed mass taking into account that the mass retained by the membrane is different from the one initially present in the feed with the following result [28]:

$$q(t).M = \delta.V.C_{in} \quad (2)$$

Where, $M$ is the mass of the membrane, $V$ is the cumulative filtrate volume, $C_{in}$ is the mass concentration of the chemical substances in feed flow, and $\delta$ is the retention rate of the membrane.

$(0 < \delta < 1)$, if $\delta = 0$: no adsorption, $\delta = 1$: total absorption

Substituting Eq. (2) in Eq. (1) leads Eq. (3):

$$\frac{d(\delta.V.C_{in}/M)}{dt} = k_n[(\frac{\delta.V.C_{in}}{M})_{max} - (\frac{\delta.V.C_{in}}{M})_t]^n \quad (3)$$

$$\frac{dv}{dt} = k_n(\frac{\delta.V.C_{in}}{M})^{n-1}.(V_m - V_t)^n \quad (4)$$

Where:

$$\begin{align*}
\left\{ \begin{array}{l}
\frac{dV(t)}{dt} = K_n(V_m - V_t)^n \\
V_{t=0} = V(0) = 0
\end{array} \right. \quad (5)
\end{align*}$$
And: $K_n = k_n \left( \frac{\delta C_m}{M} \right)^{n-1}$

2.1.1.1. Pseudo-first order equation

The pseudo order $n$ of Eq. (5) equal 1 is a simple kinetic analysis of adsorption, it is given by the following equation [29, 30]:

$$V = V_m [1 + e^{-k_1 t}] \quad (6)$$

Where, $k_1$ is the PFO rate constant of adsorption (min$^{-1}$) and $V_m$ is the filtrate volume. The constant $k_1$ model can be determined using $V$ versus $t$ plot. Fig. 2 shows a schematic representation of this variation for different concentration suspensions.

2.1.1.2. Pseudo second order equation

Where the pseudo order $n$ equal to Eq. (5) it’s based on equilibrium adsorption as the following expression of the form [31]:

$$\frac{1}{V} = \frac{1}{V_m} + \frac{1}{k_2 V^2_m \cdot \frac{1}{t}} \quad (7)$$

Where $k_2$ is the pseudo-second order rate constant (kg/g min). The filtrate volume $V$ and the constant $k_2$ can be determined experimentally from plot $V$ versus $t$ (Fig. 3).

2.1.2. Adsorption model

For the $n^{th}$ pseudo-order, the integration of Eq. (4) between the initial state ($t = 0, V = 0$) and the instantaneous state ($t = t, V = V$) is given as follows:

$$\int_{V_m}^{V_m-V} (V_m - V)^{-n} d(V_m - V) = -\int_0^t k_n dt \quad (8)$$
The integration solution of (7) has the following form:

\[ V = V_m - \left[ \frac{V_m^{n-1}}{1 + t(n-1)K_nV_m^{n-1}} \right]^{\frac{1}{n-1}} \tag{9} \]

Eq. (9) is the formula of the proposed model for the adsorption process of BSA.

The proposed model verified the following boundary conditions:

\[ \lim_{t \to 0} V = 0 \text{ and } \lim_{t \to \infty} V = V_m \]

Using origin8Pro software to indicate the parameters, respectively constant \( K_n \) and the maximum filtrate volume, according to the pseudo-order \( n \) and concentration \( C \). The relationship allows us to write the final equation of the model.

The model will be written as follows:

\[ V(t) = (1.68276 - 0.58581.n) - \left[ \frac{(1.68276 - 0.58581.n)^{n-1}}{1 + t(n-1)(\frac{N}{1.67 \times 10^{-9} + 8.64681.10^{-4})(1.68276 - 0.58581.n)^{n-1}}} \right]^{\frac{1}{n-1}} \tag{10} \]

According to the experimental data, there is an important variation of filtrate volume as a function of the concentration of adsorbed substance. In order to establish a relation between the pseudo-order of the equation and the concentration, we use the following formula Eq. (11):

\[ V(t) = V_m - \left[ \frac{V_m^{(b_0+b_1 \cdot C + b_2 \cdot C^2)-1}}{1 + t \cdot (d_0 + d_1 \cdot C + (b_0+b_1 \cdot C + b_2 \cdot C^2)-1) \cdot V_m^{(b_0+b_1 \cdot C + b_2 \cdot C^2)-1}} \right]^{\frac{1}{(b_0+b_1 \cdot C + b_2 \cdot C^2)-1}} \tag{11} \]

\[ n = b_0 + b_1 \cdot C + b_2 \cdot C^2 \]

\[ k = d_0 + d_1 \cdot C \]

\[ b_0^* = b_0 - 1 \]

After the reformulation of the new model, we finally obtain Eq. (12):
2.2. Mathematical Method

We established a MATLAB software environment program to solve the equation and optimize the parameters and make a comparison between the proposed model and other first and second-order pseudo models. In addition, our model equation is nonlinear with multi-variables and an experimental database were solved with lsqcurvefit is appropriate to solve non-linear multi-variable problems with data base and estimate the correlation coefficient between experimental data and predicted data. Lsqcurvefit used a mathematical model based on genetic and levernberg-Marquard algorithms to determine the equation parameters \( V_m, K_n \) and pseudo order \( n \), respectively by nonlinear regression and give very good adjustments to the experimental data as most of their respective regression correlation coefficients \( (R^2) \) are close to unity [31].

2.3. Error Function

Nonlinear regression has been developed as an important factor in designing the adsorption systems. However, recent works have shown the developing error (between the predictions and experimental data) and the model’s incapacity [32].

There are many ways of measuring a model’s accuracy. However, the Mean Absolute Error MAE and RMSE are ones of the many metrics for assessing the quality and efficiency of a model. The best-fit model is the one with the lowest value of MAE and RMSE, both can be range from zero to infinity [31, 33].
2.3.1. The mean absolute error (MAE)

MAE is the average of all absolute errors; it’s the difference between the experimental values and the predicted or calculated values for each instance [34] Eq. (13).

\[
MAE = \frac{1}{n} \sum_{i=1}^{n} |(Y_{i,\text{exp}} - Y_{i,\text{cal}})| \tag{13}
\]

Where \(n\) is the number of data points; \(Y_{i,\text{exp}}\) and \(Y_{i,\text{cal}}\) are referring, respectively to the experimentally and calculated values obtained from the proposed model.

2.3.2. RMSE

RMSE is a measure of performance model. It does this by measuring difference between calculated values and the experimental values, which would provide a better fit as the magnitude of the error decrease [32, 35].

\[
RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (Y_{i,\text{exp}} - Y_{i,\text{cal}})^2} \tag{14}
\]

Where \(n\) is the number of data points; \(Y_{i,\text{exp}}\) are referring to the experimental value and the \(Y_{i,\text{cal}}\) calculated values obtained from the proposed model.

3. Results and Discussion

3.1. Kinetic Model Validity

Model’s validation is the critical step in the modelling process. Thus, according to (Eq.12), PFO and PSO can follow nonlinear regression with MATLAB software. The results for adsorption of BSA are illustrated in Table 3 and the nonlinear parameters are presented in Fig. 2.

Table 3. Kinetic Parameters and Correlation Coefficients for Nonlinear Regression of PFO Equation, PSO and Model Proposed for the Adsorption of BSA on PCTE Membrane for
Different Concentration \( c = 0.5gL^{-1}, c = 1.0gL^{-1}, c = 1.4gL^{-1}, c = 2.0gL^{-1} \) and \( c = 5.0gL^{-1} \)

| Concentration | \( C = 0.5gL^{-1} \) | \( C = 1.0gL^{-1} \) | \( C = 1.4gL^{-1} \) | \( C = 2.0gL^{-1} \) | \( C = 5.0gL^{-1} \) |
|---------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|
| \( n_1(n=1) \) | 1                           | 1                           | 1                           | 1                           | 1                           |
| \( n_2(n = 2) \)   | 2                           | 2                           | 2                           | 2                           | 2                           |
| \( n_{optimal} \) | 1.1450                      | 1.5715                      | 1.1150                      | 1.9561                      | 2.0834                      |
| \( R^2_1 \)     | 0.313                       | 0.540                       | 0.255                       | 0.289                       | 0.413                       |
| \( R^2_2 \)     | 0.978                       | 0.975                       | 0.972                       | 0.989                       | 0.952                       |
| \( R^2_{optimal} \) | 0.997                      | 0.983                       | 0.993                       | 0.989                       | 0.953                       |
| \( RMSE_1 \)    | 0.285                       | 0.191                       | 0.151                       | 0.127                       | 0.074                       |
| \( RMSE_2 \)    | 0.0494                      | 0.0413                      | 0.0290                      | 0.0171                      | 0.0225                      |
| \( RMSE_{optimal} \) | 0.0208                    | 0.0364                      | 0.0171                      | 0.0171                      | 0.0215                      |
| \( MAE_1 \)     | 0.501                       | 0.298                       | 0.364                       | 0.378                       | 0.446                       |
| \( MAE_2 \)     | 0.421                       | 0.257                       | 0.419                       | 0.409                       | 0.445                       |
| \( MAE_{optimal} \) | 0.3870                    | 0.2690                      | 0.3930                      | 0.3185                      | 0.2141                      |
| \( k_1(\text{min}^{-1}) \) | 5.359                      | 8.422                       | 5.380                       | 3.792                       | 3.374                       |
| \( k_2(\text{mg}(\text{gmin})^{-1}) \) | \(8.9110^4\)          | \(1.60 10^3\)             | \(2.60 10^3\)              | \(3.10 10^3\)              | \(4.40 10^3\)              |
| \( k_{optimal} \) | \(6.69 10^4\)          | \(1.10 10^3\)             | \(1.10 10^3\)              | \(2.90 10^3\)              | \(5.00 10^3\)              |
| \( mg\text{g}^{-1}(1-n)\text{s}^{-1}) \) |                           |                             |                             |                             |                             |

A nonlinear regression with MATLAB software is performed to obtain the values of \( K_n \) and to optimize the pseudo-order \( n \) from Eq.12 when the value of filtrate volume experimental data \( V \) and time \( t \) is plotted. The different values of \( K_n \) are obtained from Eq.6, 7 and 12, respectively. For fitting the proposed model, the results of \( R^2 = 0.993 \) are obtained for concentration \( C = 1.4gL^{-1} \), optimal pseudo order equation \( n = 1.115 \) and constant...
\[ K_n = 1.11 \times 10^{-3} m\,g\,g^{-(1-n)}\,s^{-1}, \]
thus a reasonable small value of RSME and MAE also gave a good correlation between the predicted filtrate volume and experimental values. This result confirms the performance and the accuracy of the new model, which is able to describe the adsorption of BSA on PCTE membrane.

Fig. 2 presents the nonlinear regression of the calculated volume versus experimental volume. Overall, the \( R^2 \) values for PSO equation are higher than those of PFO equation but it is the best result of the new model for all the different concentrations.
Fig. 2 Nonlinear regression between experimental and calculated volume curves for five experiments 

(a) $c = 0.5 g/L$, (b) $c = 1.0 g/L$, (c) $c = 1.4 g/L$, (d) $c = 2.0 g/L$ and (e) $c = 5.0 g/L$.

3.2. Models Comparison

For more accuracy, a comparative study has been conducted between the new model (Eq. 12), the PFO (Eq. 6) and PSO (Eq. 7). However, using MATLAB software, the non-linear regression curves of the model and the PFO and PSO equations are shown in Fig. 3.
Fig. 3. Adsorption profile of BSA on PCTE membrane plotted for PFO and PSO models during five experiments (a) $c = 0.5 g/L$, (b) $c = 1.0 g/L$, (c) $c = 1.4 g/L$, (d) $c = 2.0 g/L$, (e) $c = 5.0 g/L$).

Regression results between the calculated and experimental values of the volume filtrate obtained from the PFO kinetic model did not give reasonable correlation values coefficient $R^2$ of 0.255-0.54 for different concentration of BSA, showing relatively large $RMSE$ values of 0.074-0.28. Consequently, the experimental results did not follow the first-order kinetic model.

Furthermore, for PSO kinetic, the calculated $V_{i,cat}$ values did not agree with the experimental $V_{i,exp}$ value, which also gives a relatively large deviation of $RMSE$ 0.0494-0.0171.

However, for the proposed model, the calculated $V_{i,cat}$ values were consistent with the experimental $V_{i,exp}$ values, resulting in a relatively small deviation of RMSE 0.0171–0.0364,
in addition to linear regression coefficients, close to 0.997.

Moreover, the $n$ values to the largest $R^2$ and to the least RMSE are almost identical. The value of $R^2$ obtained from the nonlinear regression of the MATLAB software can therefore be used to perfectly judge the best-fit order.

Hence, it can be concluded that the kinetics of BSA adsorption on the PCTE membrane followed the proposed model and the optimal pseudo-order equation confined between 1 and 2.

Fig. 4. Comparison of RMSE for pseudo first order equation, pseudo second order equations and the new model for five experiments ($c = 0.5 \text{ g/L, 1.0 g/L, 1.4 g/L, 2.0 g/L and 5.0 g/L}$).

3.3. Validation of the Model for Other Experimental Data in the Literature

To test the capability and validity of the proposed model, it should be possible to study the model parameters for other experimental and measurements to estimate them from correlations. In this respect, it should be collected a data possible in order to better indicate the ability of the proposed model and characterise the profile of the adsorption process. For this purpose we collect a different experimental data, the model for different experimental
cases under different conditions operational, filtration mode nature and substance adsorbed. Table 4 summarised the kinetic parameters of adsorption process for different case studies.

**Table 4.** Kinetic Parameters of MATLAB Software Results and Correlation Coefficients for Non-Linear Regression Obtained for the Case Studies and Comparison Between the New Model, PFO and PSO

| Reference | Filtrate nature | Filtration mode | Operating condition | Model | Pseudo first-order (n=1) | Pseudo second-order (n=2) |
|-----------|-----------------|-----------------|---------------------|-------|--------------------------|----------------------------|
| [36]      | DNA solution    | Membran: PVDF and PES | A\_filtration: 0.28cm\(^2\) P\_operating: 30.50 or 65 kPa T: -20°C C: 30±1μg/ml | n optim | R\(^2\) | RMSE | R\(^2\) | RMSE | R\(^2\) | RMSE |
|           |                 |                 |                     | 0.90  | 0.99 5 | 4.59 | 0.329 | 196 | 0.954 | 60.4 |
| Reference | Filtrate nature | Filtration mode | Operating condition | Model | Pseudo first-order (n=1) | Pseudo second-order (n=2) |
|-----------|----------------|----------------|---------------------|-------|-------------------------|-------------------------|
| [37]      | Oil in water emulsion | PVDF membrane | C:5000 ppm | n optim al | R² | RMSE | R² | RMSE | R² | RMSE |
|           |                |                | μ= 0.2 m/s. | 0.39 | 0.998 | 1.4×10³ | 3.6×10² | 0.16 | 0.995 | 2.3×10³ |
| [38]      | PSL membrane   | PCTE membrane | D particle: 0.522 μm | 0.8 | 0.994 | 36.9 | 0.114 | 3.14×10⁻⁴ | 0.96 | 74.6 |
|           |                |                | d : 1.05g/cm³ |                 |     |     |     |     |     |     |
|           |                |                | Pfiltration: 98- 294 kPa. |     |     |     |     |     |     |
| Reference | Filtrate nature | Filtration mode | Operating condition | Model | Statistical analysis data |
|-----------|-----------------|-----------------|---------------------|-------|--------------------------|
|           |                 |                 |                     |       | Pseudo first-order (n=1) | Pseudo second-order (n=2) |
|           |                 |                 |                     | n optim | R²  | RMSE | R²  | RMSE | R²  | RMSE |
| [39]      | IgG and NPs     | NPN membrane    | C<sub>IgG</sub>: 0.5–5 mg/mL |       |     |     |     |      |     |      |
|           |                 |                 | Concentrations of 100nm NPs: 10<sup>9</sup> up to 10<sup>13</sup> parts/mL |       |     |     |     |      |     |      |
|           |                 |                 | 20nm NPs: 10<sup>11</sup> to 10<sup>15</sup> parts/mL |       |     |     |     |      |     |      |
| [40]      | AMPS, AM and SSS | Water-based drilling fluid | T: 160°C |       |     |     |     |      |     |      |
|           |                 |                 | P: 0.69 MPa |       |     |     |     |      |     |      |
|           |                 |                 |                     |       |     |     |     |      |     |      |
Table 4 shows that the best fit orders for adsorption of DNA solution, oil in water emulsion, 2-acrylamido-2-methylpropane sulfonic acid acrylamide, sodium P-styrenesulfonate were found, respectively 0.9, 0.39, 0.8 and 0.865, and therefore they did not exceed 1. In addition, for human serum and polystyrene, the result was 1.68, thus between 1 and 2. Moreover the values of $R^2$ for the model are better than for PFO and PSO.

For the case studies, the test results show the capability of the model, it is concluded that the new model proposed can be extended for practical application.

This current work proposed a simple model to indicate the best-fit kinetic parameters for the adsorption process, which allows us to describe it more accurate than using the convenient model of pseudo-first and second-order.

4. Conclusions

The first-order and second-order pseudo models (PFO/PSO) were widely used to describe the
kinetic data of liquid/solid adsorption and the expressions of these two models were obtained based on the assumption of ideal operating conditions.

Therefore, in this study, a new model non-linear pseudo $n^{th}$ order was developed based on a real assumption, to correlate the kinetic data of BSA adsorption on PCTE membrane for different concentrations. MATLAB software was used to optimize the pseudo-order and to describe the kinetic parameters, thus a comparison of PFO, PSO and the proposed model equations for the description of adsorption kinetics has been examined.

The results indicate that the predicted values obtained from the new model are in excellent agreement with the experimental data of adsorption process giving a best correlation coefficient $R^2$ up to 0.997 and a reasonable small value of $RMSE$ and $MAE$, respectively up to 0.0171 and 0.2141 The optimal pseudo order of BSA adsorption on PCTE membrane $n = 1.115$ was between 1 and 2; the best-fit curves were plotted for the proposed model.

Depending on the capacity and validity of the model, it should be possible to study the model parameters for other experiments and measurements in order to estimate them from the correlations. In this respect, it should be collected a data possible in order to better indicate the ability of the model proposed and characterize the profile of the adsorption process. Indeed, the model gives the best fit and better correlation coefficient as first-order pseudo and second-order pseudo. Based on this work, the examination of the model parameters will be addressed in other future work.

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Nomenclature

\( A_{\text{filtration}} \) Area filtration (cm\(^2\))

\( C_{\text{in}} \) Mass substance concentration in feed flow.

\( D \) Density (g/cm\(^3\))

\( D_{\text{particle}} \) Particle diameter (\( \mu m \))

\( K_n \) Rate constant of reaction (\( mg/g(1-n)s^{-1} \))

\( k_1 \) Pseudo first order rate constant of adsorption (min\(^{-1} \)).

\( k_2 \) Pseudo second order rate constant of adsorption (mg/g min)

\( M \) Membrane mass (g).

\( MAE \) Mean relative error.

\( n \) Empirical equation order,

\( P_{\text{operating}} \) Operating pressure (KPa)

\( P_{\text{filtration}} \) Filtration pressure (KPa)

\( q \) Adsorbed amount (mg/g).

\( q_{\text{max}} \) Maximum adsorbed amount (mg/g).

\( R^2 \) Regression correlation coefficient

\( TMP \) Transmembrane pressure (KPa)

\( V \) Filtrate volume (m\(^3\)/m\(^2\))

\( V_m \) Maximum filtration volume (m\(^3\)/m\(^2\))

\( V_{\text{cal}} \) Calculated filtration volume of BSA on PCTE membrane (m\(^3\)/m\(^2\))
$V_{exp}$ Experimental filtration volume of BSA on PCTE membrane (m$^3$/m$^2$)

**Greek letters**

$\delta$ Retention rate of membrane

$\mu$ Fluid velocity (m/s)

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