Charge-Density-Excitation Spectrum in the $t$-$t'$-$J$-$V$ Model

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Abstract

We study the density-density correlation function in a large-$N$ scheme of the $t$-$t'$-$J$-$V$ model. When the nearest-neighbor Coulomb interaction $V$ is zero, our model exhibits phase separation in a wide doping region and we obtain large spectral weight near momentum $q = (0,0)$ at low energy, which originates from the proximity to phase separation. These features are much stronger for electron doping than for hole doping. However, once phase separation is suppressed by including a finite $V$, the low-energy spectral weight around $q = (0,0)$ is substantially suppressed. Instead a sharp zero-sound mode is stabilized above the particle-hole continuum. We discuss that the presence of a moderate value of $V$, which is frequently neglected in the $t$-$J$ model, is important to understand low-energy charge excitations especially close to $q = (0,0)$ for electron doping. This insight should be taken into account in a future study of x-ray scattering measurements.

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I. INTRODUCTION

Charge order and charge excitation spectra attract a renewed interest in cuprate superconductors. While the presence of spin-charge stripe order is well known in La-based cuprates, charge order discovered recently is not accompanied by spin order. Such charge order is observed not only in hole-doped cuprates (h-cuprates) such as Y$_2$Ba$_2$Cu$_3$O$_{6+\delta}$, Bi$_2$Sr$_2$CaCu$_2$O$_{y}$, and Hg-based compounds, but also in electron-doped cuprates (e-cuprates).

While charge order phenomena are now ubiquitous in cuprates, there is a clear particle-hole asymmetry between h- and e-cuprates. Charge order occurs inside the pseudogap phase in h-cuprates. In contrast, in e-cuprates the charge order is observed below 340K (Ref. 13) and seems to occur from the normal metallic phase, since the pseudogap effect is absent or very weak in this system. On the other hand, theoretical insights are controversial with regard to particle-hole asymmetry of charge excitations. A recent density-matrix renormalization group (DMRG) study for the Hubbard model with $U = 8t$ predicts an enhancement of the low-energy charge excitations in e-cuprates, whereas a similar enhancement does not occur for h-cuprates. In contrast, a leading-order theory of the large-$N$ expansion to the $t$-$J$ model shows that a tendency to charge order is stronger in h-cuprates than e-cuprates, implying that low-energy charge excitations tend to be enhanced more in h-cuprates.

These different theoretical conclusions could be understood consistently by considering the well-known insight that e-cuprates are expected to be closer to phase separation (PS) than h-cuprates as shown by various theoretical studies. However, charge excitations associated with PS are hardly known even theoretically. The proximity to PS is expected to have a strong influence on charge excitations especially near momentum $q = (0, 0)$, which will be tested by resonant inelastic x-ray scattering (RIXS) measurements in the future. Therefore it is important to clarify charge excitations close to PS. Moreover, as we will show below, PS proves to be a key to resolve the different theoretical insights obtained in Refs. 14 and 15.

In this paper, encouraged by successful explanations of the charge order and the mode near $q = (0, 0)$ in e-cuprates in terms of a large-$N$ expansion to the $t$-$J$ model, we compute the density-density correlation function in the same large-$N$ scheme as previous ones. To clarify charge excitations associated with PS, we study the impact of the nearest-neighbor Coulomb interaction $V$ and show dramatic changes of the low-energy charge...
excitations around \( q = (0,0) \) especially for electron doping. We compare our results with recent theoretical work\cite{ref14} and Ref.\cite{ref23}, both of which predict the presence of low-energy charge excitations for a small \( q \).

In Sec. 2 we describe the model and summarize the formalism. Sec. 3 contains the results which are discussed in Sec. 4. Conclusions are given in Sec. 5.

II. MODEL AND FORMALISM

Cuprate superconductors are doped Mott insulators and their minimal model is the so-called \( t-J \) model\cite{ref24,ref25}. Although the nearest-neighbor Coulomb interaction is frequently neglected in a study of the \( t-J \) model, its effect proves to be crucially important to understand charge excitations close to \( q = (0,0) \), as we will show below. Hence we study the following \( t-t'-J-V \) model

\[
H = -\sum_{i,j,\sigma} t_{ij} c_{i\sigma}^\dagger \bar{c}_{j\sigma} + J \sum_{\langle i,j \rangle} \left( \vec{S}_i \cdot \vec{S}_j - \frac{1}{4} n_i n_j \right) + V \sum_{\langle i,j \rangle} n_i n_j , \tag{1}
\]

where the sites \( i \) and \( j \) run over a square lattice. The hopping \( t_{ij} \) takes a value \( t \) (\( t' \)) between the first (second) nearest-neighbors sites. \( \langle i,j \rangle \) indicates a nearest-neighbor pair, and \( J \) and \( V \) are the spin exchange and Coulomb interaction, respectively. \( c_{i\sigma}^\dagger \) (\( \bar{c}_{i\sigma} \)) is the creation (annihilation) operator of electrons with spin \( \sigma \) (\( \sigma = \downarrow, \uparrow \)) in the Fock space without double occupancy. \( n_i = \sum_{\sigma} c_{i\sigma}^\dagger \bar{c}_{i\sigma} \) is the electron density operator and \( \vec{S}_i \) is the spin operator.

We analyze the model\cite{ref11} in terms of the large-\( N \) expansion formulated in Ref.\cite{ref26}. A full formalism is described in Ref.\cite{ref27} where charge instabilities, not charge excitations, were studied in the same framework as the present one. Hence leaving the details to Sec. II A in Ref.\cite{ref27}, we here keep our presentation minimal. In the large-\( N \) approach, charge excitations with momentum \( q \) and bosonic Matsubara frequency \( \omega_n \) are described by a \( 6 \times 6 \) bosonic propagator

\[
D_{ab}^{-1}(q, i\omega_n) = [D_{ab}^{(0)}(q, i\omega_n)]^{-1} - \Pi_{ab}(q, i\omega_n) . \tag{2}
\]
Here \(a\) and \(b\) run from 1 to 6, \(D_{ab}^{(0)}(\mathbf{q}, i\omega_n)\) is a bare bosonic propagator

\[
[D_{ab}^{(0)}(\mathbf{q}, i\omega_n)]^{-1} = N \begin{pmatrix} F(q) & \frac{\delta}{2} 0 & 0 & 0 & 0 \\ \frac{\delta}{2} & 0 0 0 0 0 \\ 0 0 4\Delta^2 & 0 & 0 \\ 0 0 0 4\Delta^2 & 0 \\ 0 0 0 0 4\Delta^2 & 0 \end{pmatrix},
\]

and \(\Pi_{ab}(\mathbf{q}, i\omega_n)\) are self-energy corrections at leading order; \(F(q) = (\delta^2/2)[V(q) - J(q)]\), \(V(q) = V(\cos q_x + \cos q_y)\) and \(J(q) = \frac{\delta}{2}(\cos q_x + \cos q_y)\); for a given doping rate \(\delta\), the mean-field value of a bond-field \(\Delta\) is determined self-consistently.

We compute the density-density correlation function in the present large-\(N\) scheme. Summing all contributions up to \(O(1/N)\), we obtain

\[
\chi^c(\mathbf{q}, i\omega_n) = N \left(\frac{\delta}{2}\right)^2 D_{11}(\mathbf{q}, i\omega_n).
\]

Thus, the density-density correlation function is connected with the component \((1, 1)\) of the \(D_{ab}\). The factor \(N\) in front of Eqs. (3) and (4) comes from the sum over the \(N\) fermionic channels after the extension of the spin index \(\sigma\) from 2 to \(N\).

Although the physical value is \(N = 2\), the large-\(N\) expansion has several advantages over usual perturbation theories. First, charge degrees of freedom are generated by carrier doping into a Mott insulator and thus the effect of the Coulomb interaction should vanish at half-filling. This feature is not reproduced in weak coupling theory\(^{28}\) but in the present leading order theory; see the \((1, 1)\) component in Eq. (3). Second, the large-\(N\) expansion yields results consistent with those obtained by exact diagonalization for charge excitations\(^{29}\) including plasmons\(^{22,30}\). As we will discuss later, the present formalism also predicts charge excitations similar to those obtained in the dynamical DMRG method\(^{14}\). Third, we actually showed that the present large-\(N\) framework can capture short-range charge order recently observed by resonant x-ray scattering\(^{13,21}\) and also a mysterious mode around \(\mathbf{q} = (0, 0)\) observed by RIXS for \(e\)-cuprates\(^{19,20,22}\).
FIG. 1: (Color online) (a)-(c) $q$-$\omega$ maps of $\text{Im}\chi^c(q, \omega)$ at $T = 0$ and $\delta = 0.20$ for several choices of Coulomb repulsion $V$. $q$ is scanned along the symmetry axes: $(\pi, \pi) \rightarrow (0, 0) \rightarrow (\pi, 0) \rightarrow (\pi, \pi)$. (d) $q$-$\omega$ map of $\text{Im}\chi^c(q, \omega)$ in the same condition of (a), except that a sign of $t' (= -0.3)$ is changed to mimic the hole-doped case.

III. RESULTS

As it is well known\textsuperscript{15–18}, a tendency toward PS is stronger for $e$-cuprates than $h$-cuprates. We therefore choose parameters appropriate to $e$-cuprates\textsuperscript{21} such as $J/t = 0.3$ and $t'/t = 0.3$. Hereafter all quantities with dimension of energy are measured in units of $t$. We compute $\text{Im}\chi^c(q, \omega)$ after analytical continuation in Eq. (4)

\[ i\omega_n \rightarrow \omega + i\Gamma, \]

where $\Gamma(> 0)$ is infinitesimally small and we set $\Gamma = 10^{-2}$ for numerical convenience. Temperature $T$ is fixed at $T = 0$. Since PS occurs below $\delta_c = 0.18$ in the present parameters for $V = 0$ [see the inset of Fig. 2 (a)], we choose the doping $\delta$ as $\delta = 0.20$, which is in the paramagnetic phase but close to PS.

Figure 1 shows intensity maps of $\text{Im}\chi^c(q, \omega)$ for several choices of $V$ along the symmetry
axes: \((\pi, \pi) \rightarrow (0, 0) \rightarrow (\pi, 0) \rightarrow (\pi, \pi)\). The dotted line denotes the upper bound of particle-hole excitations, above which there is a sharp dispersive mode. This is a particle-hole bound state, called as the zero-sound mode. The zero-sound mode was actually obtained in different approximations to the \(t-J\) model\cite{26,33,34}. Since it is a sound wave, it features a gapless linear dispersion around \(\mathbf{q} = (0, 0)\). For \(V = 0\) [Fig. 2(a)], there exists large low-energy spectral weight inside the particle-hole continuum slightly below the zero-sound mode around \(\mathbf{q} = (0, 0)\). This low-energy spectral weight diverges upon approaching the PS boundary \(\delta_c\), leading to the divergence of the compressibility there. Therefore this low-energy spectral weight originates from the proximity to PS. Because of the mixture of the large low-energy spectral weight, the zero-sound mode is overdamped around \(\mathbf{q} = (0, 0)\) and becomes less clear. By introducing \(V\), PS is suppressed as expected [see the inset of Fig. 2(a)]. Concomitantly low-energy spectral weight around \(\mathbf{q} = (0, 0)\) is also suppressed as shown in Figs. 2(b) and (c) for \(V = 0.5\) and \(V = 1\), respectively. We then obtain only the zero-sound mode as dominant charge excitations around \(\mathbf{q} = (0, 0)\).

FIG. 2: (Color online) (a) \(\omega\) dependence of \(\text{Im} \chi^c(\mathbf{q}, \omega)\) at \(\mathbf{q} = (\pi/7, \pi/7)\) and (b) \(\mathbf{q}\) dependence of the integrated spectral weight with respect to \(\omega(>0)\) for \(V = 0, 0.2, \cdots, 1.0\). The inset in (a) shows the \(V\) dependence of the critical doping, below which PS occurs at \(T = 0\), whereas the inset in (b) the \(V\) dependence of the total spectral weight integrated over \(\omega(>0)\) and \(\mathbf{q}\) along \((\pi, \pi) \rightarrow (0, 0) \rightarrow (\pi, 0) \rightarrow (\pi, \pi)\).
Details of the \( V \) dependence of the spectral weight are presented in Fig. 2(a) as a representative, where we present \( \text{Im} \chi^c(q, \omega) \) at low momentum \( q = (\pi/7, \pi/7) \) for various choices of \( V \). With increasing \( V \), the spectral weight is transferred to a high energy region and the peak associated with the zero-sound mode is enhanced. However, when the spectral weight is integrated for each \( q \) with respect to energy \( (> 0) \), such \( q \)-resolved total spectral weight \( S(q) \), which corresponds to the equal-time correlation function at \( T = 0 \), is suppressed around \( q = (0, 0) \) with increasing \( V \) as shown in Fig. 2(b). This suggests that the contribution from the proximity to PS is indeed sizable in the spectral weight around \( q = (0, 0) \). The spectral weight is mainly transferred to a region around \( q = (\pi, \pi) \). This is because a large \( V \) favors a checkerboard-type charge-density-wave. In fact, such charge order would occur for \( V > V_c \approx 2.1 \), but we consider that the region of \( V < V_c \) is relevant to cuprate superconductors. On the other hand, the total weight integrated over \( \omega(> 0) \) and \( q \) along the symmetry axes \( (\pi, \pi) \rightarrow (0, 0) \rightarrow (\pi, 0) \rightarrow (\pi, \pi) \) does not depend on \( V \) [see the inset in Fig. 2(b)]. Therefore the spectral weight around \( q = (0, 0) \) is transferred to the region around \( q = (\pi, \pi) \) with increasing \( V \). This spectral weight transfer occurs already for \( V \) much smaller than \( V_c \) and we do not observe any charge dynamics, which could be associated with other types of charge orders such as stripes from the mechanism of frustrated PS.

For the hole-doped case, we may change the sign of \( t' \). In this case, the tendency toward PS becomes much weaker than that for a positive \( t' \). As seen in Fig. 2(d), there is no enhancement of low-energy spectral weight around \( q = (0, 0) \) even for \( V = 0 \). In fact, there occurs no PS for any doping. Hence the effect of \( V \) becomes much weaker around \( q = (0, 0) \). However, the tendency toward charge order at \( q = (\pi, \pi) \) is common to both sign of \( t' \) for a large \( V \).

IV. DISCUSSIONS

We have found that the nearest-neighbor Coulomb repulsion \( V \) plays a crucial role to understand the low-energy charge excitations around \( q = (0, 0) \) especially in a model calculation for \( e \)-cuprates, because \( e \)-cuprates are expected to be close to PS.

Recently low-energy charge excitations were reported by a DMRG method for a \( 6 \times 6 \) cluster of the Hubbard model with \( U = 8t \) (Ref. 14). In particular, the presence of the low-energy peak was predicted in \( e \)-cuprates at energy lower than the currently available
RIXS data\ref{14}.

The Hubbard model with a large $U$ should share similar properties to the $t$-$J$ model and indeed exhibits phase separation\ref{18,37}. Hence the predicted low-energy charge excitations likely originate from the proximity to PS and would be strongly suppressed once the Coulomb repulsion is included. To demonstrate the connection between the present work and Fig. 4 in Ref. \ref{14}, we took the same momenta, doping, and a large damping $\Gamma = 0.1t$ to mimic the broadening of Ref. \ref{14}. $V$ is set to zero. We then computed $\text{Im}\chi_c(q,\omega)$ within the present theory for both $t' = 0.3t$ (electron-doped case) and $t' = -0.3t$ (hole-doped case). Since a large $\Gamma$ was invoked, PS does not occur even for the electron-doped case in our framework, but charge fluctuations associated with the proximity to PS are expected.

Figures \ref{fig:3}(a) and (b) capture major features of Figs. 4(c) and (d) in Ref. \ref{14}, respectively. The low-energy spectral weight is strongly suppressed at $q = (\pi/7, 2\pi/3)$ and $(\pi/7, \pi)$ in Fig. \ref{fig:3}(a), but there is strong enhancement in a low-energy region at $q = (\pi/7, \pi/3)$. In the hole-doped case [Fig. \ref{fig:3}(b)] the low-energy spectral weight is substantially suppressed at $q = (\pi/7, 2\pi/3)$ and $(\pi/7, \pi)$, similar to the corresponding results in the electron-doped case [Fig. \ref{fig:3}(a)]. At small momentum $q = (\pi/7, \pi/3)$, low-energy spectral weight is enhanced more than at $q = (\pi/7, 2\pi/3)$ and $(\pi/7, \pi)$, because of the presence of zero-sound mode at relatively low energy [see Fig. \ref{fig:1}(d)]. In a lower energy region ($2\omega/t \lesssim 0.4$), we just
see the tail of the zero-sound mode and do not observe the enhancement of the spectral weight as that seen in the electron-doped case [Fig. 3(a)]. This contrast of low-energy charge excitations between the electron- and hole-doped case originates from the proximity to PS in the former case. In fact, once $V$ is introduced, such low-energy spectral weight is substantially suppressed and both electron- and hole-doped cases show similar charge excitations at low energy for a small $\mathbf{q}$, as we have already seen in Fig. 1. Low-energy charge excitations at small $\mathbf{q}$ are also reported in the $t$-$J$ model with $t' = 0$ and $V = 0$ in Ref. 23. Such excitations may also come from the proximity to PS.

The zero-sound mode is stabilized in the present model, consistent with the literature. We have found that the presence of the zero-sound mode is independent of the value of $V$. Recalling our parameters $J = 0.3$ and $0 \leq V \leq 1.0$, the effective interaction $V(\mathbf{q}) - J(\mathbf{q})$ in the $(1, 1)$ component of Eq. (3) changes a sign at $V = 0.15$. Moreover because of the form factor, $\cos q_x + \cos q_y$, the sign of $V(\mathbf{q}) - J(\mathbf{q})$ depends on $\mathbf{q}$. Nevertheless, the zero-sound mode is stabilized for any $V$ and $\mathbf{q}$ in Fig. 1. In fact, as shown in Refs. 32 and 34, the zero-sound exists even for $J = V = 0$. This cannot be understood in terms of a usual weak coupling analysis such as a random phase approximation (RPA).

Instead, the robustness of the zero-sound mode originates from strong correlation effects contained in the $t$-$J$ model in the sense that the present leading order theory does not predict a RPA-like susceptibility, but predicts

$$\chi^c(\mathbf{q}, \omega) \sim \frac{\Pi_{22}(\mathbf{q}, \omega)}{[2F(\mathbf{q}) - \Pi_{11}(\mathbf{q}, \omega)]\Pi_{22}(\mathbf{q}, \omega) + [\delta - \Pi_{12}(\mathbf{q}, \omega)]^2}.$$  \hfill (6)

Here we have neglected the components $\alpha, \beta = 3, 4, 5, 6$ in Eqs. (2) and (3), and their contributions are actually minor. We can check that the dispersion of the zero-sound mode is determined by the condition

$$[2F(\mathbf{q}) - \text{Re}\Pi_{11}(\mathbf{q}, \omega)]\text{Re}\Pi_{22}(\mathbf{q}, \omega) + [\delta - \text{Re}\Pi_{12}(\mathbf{q}, \omega)]^2 = 0.$$  \hfill (7)

The point is that the term, $2F(\mathbf{q}) - \text{Re}\Pi_{11}(\mathbf{q}, \omega)$, is always positive in the parameter space we have studied and $\text{Re}\Pi_{22}(\mathbf{q}, \omega)$ is negative at high energy. Equation (7) is then fulfilled. This is the reason why the zero-sound mode is robust in the present model. We may interpret high-energy peaks of the density-density correlation function obtained by exact diagonalization as the zero-sound mode, as pointed out in Refs. 32 and 33.

The robustness of the zero-sound mode, however, should be taken carefully. In fact the zero-sound mode changes to a plasmon mode with an excitation gap at $\mathbf{q} = (0, 0)$ by...
including the long-range Coulomb interaction, as recently shown in the present large-$N$ scheme for a layered system\textsuperscript{22}.

The strong asymmetry of PS between $e$-cuprates ($t' > 0$) and $h$-cuprates ($t' < 0$) is also understood from Eq. (6). To simplify our analysis, we put $V = J = 0$, i.e., $F(q) = 0$. We then obtain at $T = 0$

$$\chi^c(q \to 0, \omega = 0) \sim \frac{N_F}{\delta - 4\mu N_F},$$

where $N_F$ is the density of states at the Fermi energy and $\mu$ is the chemical potential\textsuperscript{27}. Hence PS occurs when the following condition is fulfilled:

$$\delta < 4\mu N_F.$$  \hspace{1cm} (9)

We can check that $\mu$ becomes positive close to half-filling only for $t' > 0$ and Eq. (9) is fulfilled, showing that PS can occur only for the electron-doped case. We can also check that Eq. (9) indeed explains our previous numerical results, Fig. 3(a) for $V = J = 0$ in Ref. \textsuperscript{15}. Therefore the asymmetry of PS between $e$- and $h$-cuprates is controlled by Eq. (9) and originates from strong correlation effects in the sense that Eq. (9) is obtained for $V = J = 0$. For a finite $J$ and $V$ we can perform a similar analysis and obtain the same conclusion.

V. CONCLUSIONS

We have studied charge excitations in the $t$-$t'$-$J$ model by including the nearest-neighbor Coulomb repulsion $V$. While the effect of $V$ is frequently neglected in research of charge excitations in cuprates, we have found that the $V$ term is crucially important to understand low-energy charge excitations around $q = (0, 0)$ [Figs. 1(a)-(c) and 2(a)] especially in a model calculation for $e$-cuprates. In line with the prediction in Ref. \textsuperscript{14}, we have also obtained low-energy spectral weight around $q = (0, 0)$, but this comes from the proximity to PS and holds only if the effect of $V$ is sufficiently small. Given the increasing interest in the study of low-energy charge excitations around $q = (0, 0)$ in RIXS, it is crucial to consider the presence of the Coulomb repulsion, which is expected to be finite in real systems. We have also found that the zero-sound mode is stabilized above the particle-hole continuum, which is independent of a value of $V$. 

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