Fayans functional for deformed nuclei. Uranium region.

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Abstract. Fayans energy density functional (EDF) FaNDF\textsuperscript{0} has been applied to the nuclei around uranium region. Ground state characteristics of the Th, U and Pu isotopic chains, up to the two-neutron drip line, are found and compared with predictions from several Skyrme EDFs. The two-neutron drip line is found for FaNDF\textsuperscript{0}, SLy4 and SkM* EDFs for a set of elements with even proton number, from Pb up to Fm.

1 Introduction

Presently, the Hartree-Fock (HF) or Hartree-Fock-Bogoliubov (HFB) methods together with the effective Skyrme forces \textsuperscript{1}. Gogny forces \textsuperscript{2} or relativistic mean-field (RMF) models \textsuperscript{3} are most common microscopic models applied for description of the ground state properties of the heavy nuclei. All of the aforementioned approaches are usually interpreted as a version of the energy density functional (EDF) method suggested by Kohn and Sham \textsuperscript{4}. This method is based on the theorem of Hohenberg - Kohn \textsuperscript{5}, which states that the ground state energy $E_0$ of any quantum system is a functional of its density $\rho \!(\!r\!)$). By itself, the theorem says nothing about the form of this functional, and various options for the Skyrme EDF and the Gogny EDF are, in fact, different “ansatzs”.

Among popular Skyrme EDFs, there are quite old functionals SkM* \textsuperscript{6} and SLy4 \textsuperscript{7}, see the review article \textsuperscript{8}. A record in the accuracy of the description of the nuclear masses belongs to the Skyrme functional HFB-17 \textsuperscript{9} with the average deviation from the experiment being around 600 keV, obtained by adding phenomenological corrections atop of the mean-field. Of a comparable accuracy are the other functionals of this family, up to the HFB-27, the corresponding tables are presented on the site \textsuperscript{10}. Also relatively new functional UNEDF1 \textsuperscript{11} has proved to be very successful in describing the deformed nuclei.

It is also worth to mention a relatively newly developed approach, known originally as a BCP (Barcelona - Catania - Paris) \textsuperscript{12} method, and later as a BCPM (Barcelona - Catania - Paris - Madrid) method \textsuperscript{13}. The main bulk term of the BCPM functional was found by starting from the equation of the state of nuclear and neutron matter, obtained within the Brueckner–Hartree–Fock method by using a realistic $NN + NNN$ potential.

We use the EDF developed by S.A. Fayans with coauthors \textsuperscript{14–17}. In comparison to the Skyrme or Gogny EDFs, it possess two main peculiarities. Firstly, the main in-volume term of the Fayans EDF has more sophisticated form. It can be schematically written as

$$E(\rho) = \frac{a\rho^2}{2} \left( 1 + \alpha \rho^t \right) + \frac{b}{1 + \gamma \rho^s}.$$  (1)

The corresponding term of the Skyrme EDF would correspond to $\gamma=0$ case within this relation. The use of the bare mass, $m^*=m$, is another peculiarity of the Fayans method. Both features of this approach are closely related to the self-consistent Theory of Finite Fermi Systems (TFFS) \textsuperscript{18}. The latter is based on general principles of the TFFS \textsuperscript{19}, supplemented with the TFFS self-consistency relations \textsuperscript{20}. These two peculiarities of the Fayans approach reflect, in an effective manner, energy dependence effects inherent to the self-consistent TFFS. E.g., the effective mass in this approach is a product $m^*=m^*_e \cdot m^*_f$ of the “$k$-mass” and the “$E$-mass”. The two effects compensate each other almost exactly \textsuperscript{18} resulting in $m^*=1$. In the Skyrme HF method, the $E$-mass is identically equal to unity and the effective mass may deviate from unity.

Until recently, the Fayans method was applied for spherical nuclei only. It turned out to be rather successful in systematic description of nuclear magnetic \textsuperscript{21, 22} and quadrupole \textsuperscript{23, 24} moments, nuclear radii \textsuperscript{25}, beta-decay probabilities \textsuperscript{26}, the energies and $B(E2)$ values for the first excited $2^+$ states in semi-magic nuclei \textsuperscript{27, 28}. In a recent study of the single-particle energies in seven magic nuclei, a record accuracy was achieved \textsuperscript{29}. Most of these calculations were made with the EDF DF3-a \textsuperscript{30}, which is a small modification of the DF3 \textsuperscript{15, 17} param-

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eter set, concerning the spin-dependent terms of the EDF. In particular, the effective tensor term of DF3-a is significantly stronger than the DF3 one.

The Fayans EDF was applied recently to deformed nuclei for the first time [31]. A localized version FaNDF0 [16] of the general finite range Fayans EDF was used which makes its surface term more similar to the Skyrme one. This allowed to employ the computer code HF-BTHO [32], developed for Skyrme EDFs, with some modifications.

The results obtained with the FaNDF0 EDF for Pb and U isotopic chains turned out to be promising. In the present work, we continue these calculations around the uranium region. In particular, we investigate the two-neutron drip line for a set of elements from Pb up to Fm, those with even proton number being considered. For completeness, we included also into the analysis predictions from the HFB-17 and HFB-27 functionals taken from Ref. [10]. In addition we discuss deformation characteristics of the drip line nuclei.

Recent interest to the problem of fixing the neutron drip line [33, 34] is partially induced with importance of this characteristic of the nuclear chart for analysis of the r-process dynamics in stars [35–37]. A couple of remarks should be made concerning validity of the EDF method with fixed set of parameters for predicting the drip lines. In particularly for the older generation EDFs, the parameterizations were obtained by using data on nuclei close to the stability, that is, with the chemical potential $\mu_{n,p}=8\text{ MeV}$. When extrapolating to very neutron rich systems, the role of EDF parameter errors becomes prominent [33, 38]. Also, analysis of the problem on the basis of the many-body theory point of view [39, 40] shows that in vicinity of drip lines, that is $\mu_n \to 0$ or $\mu_p \to 0$, the EDF parameters describing the effective NN-interaction at the nuclear surface may need to be modified. Close to the neutron drip line, with a small chemical potential $\mu_n$, attractive part of the NN-interaction may become enhanced, resulting a deeper neutron mean field. This, as a consequence, shifts the drip line farther away. To take this effect into account, a simple model was used in [33, 40] which, evidently, overestimates the effect, predicting unrealistically strong shift of the drip line. It was, nevertheless, demonstrated that this effect shifts the drip line. However, one should bear in mind that by explicitly introducing such kind of component to the EDF model, the model parameters need to be readjusted, which, so far, has not yet been done. Thus, the total net effect remains still unknown. In the present work we use the standard approach with fixed EDF parameters.

2 Deformation properties of Th, U, and Pu isotopic chains

Details of the computation scheme are identical to those described in [31]. We employ the axial computer code with the oscillator basis, the number of the oscillator shells being equal to $N_{sh}=25$. We limit ourselves to the quadrupole deformation $\beta_2$ only, with reflection symmetry assumed. All the parameters of the normal component of the used FaNDF0 EDF are the same as in [16]. As for the anomalous term of the EDF [16],

$$E_{anom} = \sum_{i=\alpha,p} v_i^a (r) F^a (\rho_i (r)) v_i (r),$$

where $v_i (r)$ is the anomalous density, a simplified version is used,

$$F^a (\rho_i) = C_0 \left( f_{\text{ex}}^{\text{c}} + h^{F_i} (\rho_i / \rho_0) \right).$$

Here $\rho_i = \rho_0 + p$, and $C_0 = \pi^2 / \rho m$ is the usual for TFFS normalization factor. The HFB equations are solved by using quasi-particle cut-off energy $E_{\text{cut}} = 60\text{ MeV}$. The main part of calculations are carried out by employing simplest (“volume”) model of pairing, $h^{F_i} = 0$, with $f_{\text{ex}}^{\text{c}} = -0.440$. All calculations are repeated for two Skyrme EDFs, SKM* and SLy4, the results being compared also with predictions [10] from another two Skyrme EDFs, HFB-17 and HFB-27 EDFs.

Let us begin from the uranium chain. The two-neutron separation energies,

$$S_{2n} (N,Z) = B (N,Z) - B (N-2,Z),$$

are displayed in Fig. 1. Here $B (N,Z)$ is the binding energy of the nucleus under consideration. Comparison is
made with experimental data [41] and predictions from four Skyrme EDFs. We first consider region of $A \leq 244$ with known experimental values. The HFB-17 and HFB-27 models reaffirm their high accuracy. As to the FaNDF\(^0\) functional, agreement also looks rather reasonable, taking into account that the parameters were fitted \[16\] only for spherical nuclei not heavier than lead. The deviation of 0.5 MeV from the experimental $S_{2\alpha}$ values for heavy U isotopes is explained mainly by two reasons, with the use of a simple volume pairing interaction, and absence of the effective tensor term in the FaNDF\(^0\) EDF. Indeed, as it was shown in \[30\], the tensor term is especially important in uranium and transuranium region as, in corresponding spherical case, high-$j$ levels dominate in vicinity of the Fermi level for these nuclei. As a result, the spin-orbit density, which comes to the EDF together with the tensor force, is typically large in these nuclei, changing significantly along the isotopic chain. For the SLy4 EDF agreement is a bit worse, whereas the disagreement is more significant in the SKM* case. It is worth to note that this Skyrme EDF, being fitted to masses not with so high accuracy as some modern equivalents, reproduces e.g. fission properties in actinides or energies and $B(2\epsilon)$ values of the first excited $2^+$ states in semi-magic nuclei \[42\] relatively well. For higher $A$ values the SKM* values of $S_{2\alpha}$ are significantly higher than those for all other EDFs. As a result the corresponding drip line point $A_{2\alpha}^{drip} \approx 320$ turns out be significantly farther away than for all other EDFs. This quantity is defined as the last nucleus for which the two-neutron separation energy is yet positive. For SLy4 we note that $S_{2\alpha}$ at $A = 286$ is slightly negative. However, after this point the $S_{2\alpha}$ remain positive up to $A = 298$. This kind binding re-entrance was also predicted at \[53\]. Thus, we can set $A_{2\alpha}^{drip}(\text{SLy4}) = 298$.

The ground state quadrupole deformation parameter $\beta_2$ of the U chain and the corresponding deformation energy,

$$E_{\text{def}}(\beta_2) = B(\beta_2) - B(\beta_2 = 0),$$

are displayed in Figs. \[2\] and \[3\] correspondingly. Here, each curve is cut around the corresponding drip point. Generally, all five EDFs under discussion behave in similar way, the most of nuclei in this chain being deformed in a prolate way whereas there exists a region of spherical nuclei around $A \approx 280$. In more detail, the width of the spherical region is narrowest for the FaNDF\(^0\) EDF and widest for SLy4. Both of the HFB EDFs predict oblate deformations for four nuclei $262 \leq A \leq 268$, whereas the FaNDF\(^0\) EDF, only for two of them, $A = 264$ and $A = 266$.

The reason for this difference is quite simple. In vicinity of the phase transition, with a change of the deformation sign, there are typically two energetically close by minima, the prolate and oblate one. Their closeness may be confirmed with the observation that the deformation energy, see Fig. \[3\] does not show any non-regular behavior in the transition point, where the order of two minima changes. In such kind of situation, the transition value of $A$ may move even due to a small change of the EDF parameters. In the mass region of $A > 280$ the prolate deformation arises for the FaNDF\(^0\) EDF for three points earlier than for both HFB and SLy4 EDFs. In this region the maximum value of $\beta_2 = 0.25$ appears for FaNDF\(^0\) EDF just in the drip line point. The corresponding value is a bit less for the HFB-17 EDF, being $\beta_2 \approx 0.2$ for other three EDFs. The difference is greater for the deformation energy due to its quadratic behavior around the minima. Thus, all five EDFs under consideration predict a well developed prolate deformation for uranium isotopes in the vicinity of the drip line.

Next, we investigate the thorium chain. The two-neutron separation energies are displayed in Fig. \[4\]. Again, all EDFs, with exception of SKM*, behave in general similarly in the region of $A \leq 280$, the latter curve being significantly higher. Close to the drip line, however, the picture is different. In accordance with the above discussion, binding re-entrance can be now seen also for FaNDF\(^0\). As a result, we obtain $A_{2\alpha}^{drip}(\text{FaNDF}^0) = 294$. For the HFB-17 and HFB-27 EDFs, the drip points are $\approx 300$ whereas again the highest value $A_{2\alpha}^{drip} = 306$ there is for the SKM* EDF.

The ground state deformation parameter $\beta_2$ of the Th chain and the corresponding deformation energy are displayed in Figs. \[8\] and \[9\] correspondingly. Again all five EDFs lead to similar results until $A \approx 280$, and there is rather extended region of spherical nuclei around this point. For all EDFs under consideration, the positive deformations appear in the drip region, the values of deformation parameter reaching $\beta_2 \approx 0.2$.  

Figure 3. $E_{\text{def}}$ values in the uranium chain for different EDFs.

Figure 4. $S_{2\alpha}$ values in the thorium chain for different EDFs.
other EDFs confirm it. Again, this disagreement is a region of oblate deformations at 266 correspondingly. The HFB-17 and HFB-27 EDF reveal a deformation parameter \( \beta \) in the thorium chain. The two-neutron separation energies are shown in Fig. 7.

Lastly, we investigate the plutonium isotopic chain. The two-neutron separation energies are shown in Figs. 8 and 9. Similarly as in the uranium chain, all the EDFs under consideration lead to a strong prolate deformations in the drip line region, and again the FaNDF\(^2\) deformation is the largest one.

3 Two-neutron drip line

In this section, we analyze the two-neutron drip line for a set of elements with an even \( Z \) value, from Pb up to Fm. These nuclei are important for analysis of the \( r \)-process in stars \([35,37]\). As in the previous Section, we compare predictions from the FaNDF\(^2\) functional with those from four Skyrme EDFs. The results are presented in Table 1. The values in the SLy4 and SKM* columns are found using the code \([32]\). They coincide or are very close to the corresponding results presented in \([33]\). Small differences can be explained with some distinctions in the calculation details, for example by the number of used oscillator shells. The values in HFB-17 and HFB-27 are taken from \([10]\). For each \( A_{\text{2n}} \), the corresponding value of the deformation parameter is given in brackets. We see that the major part of the EDFs under consideration predict a spherical form for the drip line nuclei in the region from Pb until Ra, whereas all of them, from Th and heavier, are deformed.

As a rule, predictions from the SKM* EDF are significantly higher compared to others. The difference is especially large for Rn and Ra elements for which this EDF predicts a strong deformation in the drip line region, whereas these nuclei remain to be spherical for other EDFs. For the SKM* EDF, a strong irregularity in the sequence of a competition of two close by energy minima, as was discussed earlier. For HFB-17 and HFB-27 EDFs, the oblate minimum has lower energy, whereas for other EDFs, the prolate minimum has a lower energy. Similarly as in the uranium chain, the spherical region ends for the FaNDF\(^2\) EDF a bit earlier than for others. One more peculiarity occurs for the Fayans EDF: after the last spherical nucleus \(^{280}\text{Pu}\), a small oblate deformation \( \beta \approx 0.05 \) appears in \(^{282}\text{Pu}\), which than becomes prolate deformed, \( \beta \approx 0.1 \) in \(^{285}\text{Pu}\). In this case, there is a competition of three close by minima, a spherical one and two deformed ones. The spherical minimum is lowest in \(^{280}\text{Pu}\), the oblate one in \(^{282}\text{Pu}\) and the prolate minimum in \(^{284}\text{Pu}\). Note that such a small negative deformation in \(^{280}\text{Pu}\) is almost invisible in the deformation energy curve, in Fig. 9. Similarly as in the uranium chain, all the EDFs under consideration lead to a strong prolate deformations in the drip line region, and again the FaNDF\(^2\) deformation is the largest one.
Table 1. Two-neutron drip line points $A_{2n}^{drip}(Z)$, from Pb to Fm, for different EDFs. In addition, the deformation $\beta_2$ of the drip line nucleus is given in brackets.

| element | FaNDF$^0$ | SLy4 | SkM* | HFB-17 | HFB-27 |
|---------|-----------|------|------|--------|--------|
| Pb      | 266 [0.00]| 266  | 272  | 266    | 266    |
| Po      | 270 [0.00]| 272  | 280  | 268    | 268    |
| Rn      | 268 [0.00]| 274  | 298  | 272    | 274    |
| Ra      | 272 [0.00]| 276  | 304  | > 286  | > 286  |
| Th      | 294 [0.24]| 292  | 306  | 300    | 298    |
| U       | 300 [0.26]| 298  | 318  | 308    | 304    |
| Pu      | 308 [0.27]| 304  | 324  | 314    | 310    |
| Cm      | 312 [0.28]| 310  | 336  | 320    | 316    |
| Cf      | 318 [0.27]| 316  | 354  | 324    | 322    |
| Fm      | 324 [0.26]| 322  | 342  | 330    | 328    |

**Figure 9.** $E_{def}$ values in the plutonium chain for different EDFs.

$A_{2n}^{drip}(Z)$ dependence occurs for Cf. The anomalously high value of $A_{2n}^{drip}$ (SKM*) is explained with the competition between the spherical and prolate minima of the total energy, the spherical one being lower, whereas the prolate ones are lower in all the neighboring elements. The predictions from the HFB-17 and HFB-27 EDFs are, as a rule, rather close to each other. The maximal difference between the corresponding values of $A_{2n}^{drip}$ equals to 4. As to the FaNDF$^0$ predictions, they turned out to be very close to those of the SLy4 EDF. The difference between them and both HFB EDFs is also quite moderate.

A remark should be made concerning the relation between $A_{2n}^{drip}$ values and one-neutron drip line points $A_{n}^{drip}$. Usually, due to the pairing effect, the inequality $A_{n}^{drip} \leq A_{2n}^{drip}$ is valid [33, 54].

Finally, we would like to stress, that in particularly such a heavy region of the nuclear chart, extrapolation of current EDF models up to the drip line is prone to large uncertainties. Therefore, the results presented here should be taken with a typical uncertainty bar of ±10 mass units, or more [33]. An additional shift of the two-neutron drip line may occur due to the effect of $\mu$-dependence of the EDF parameters [39, 40], as discussed in the Introduction.

**4 Conclusions**

Fayans energy density functional FaNDF$^0$ is applied to nuclei around the uranium region. For Th, U, and Pu isotopic chains, the two-neutron separation energies $S_{2n}$, the ground state quadrupole deformation parameter $\beta_2$ and the corresponding deformation energies $E_{def}(\beta_2)$ are found and compared with predictions from several Skyrme EDFs. Those from the SLy4 and SkM* EDFs were calculated by using the code [32], whereas the HFB-17 and HFB-27 predictions are taken from [10]. For the major part of nuclei with known experimental $S_{2n}$ values, the results obtained with the Fayans and SLy4 EDFs are rather close to those with two HFB EDFs, the HFB-17 one being highly accurate in the overall description of nuclear masses [34]. The SkM* EDF overestimates $S_{2n}$ values leading for these three elements to the two-neutron drip line point $A_{2n}^{drip}$ values noticeably higher than those obtained with the other EDFs under consideration. The deformation characteristics, the deformation parameter $\beta_2$ and the corresponding deformation energy $E_{def}(\beta_2)$, for the FaNDF$^0$ EDF, are also in the overall agreement with those of SLy4 and two the HFB EDFs. The SkM* predictions are again different, especially around the drip line region.

The two-neutron drip line is found for FaNDF$^0$, SLy4 and SkM* EDFs for a set of elements with even proton number, from Pb up to Fm. This part of the nuclear chart is important for the study of the r-process in stars [35–37]. The consideration is made within a standard approach with fixed EDF parameters found mainly for stable nuclei. Within such approach, there is an overall agreement between all EDFs under consideration except SkM*, the latter predicting sufficiently higher $A_{2n}^{drip}$ values.

To conclude, the ground state properties of deformed nuclei in the uranium region, predicted from the FaNDF$^0$ EDF, are found to be rather similar to those from several popular Skyrme EDFs. The same also holds for the prediction of the two-neutron drip line for even proton number elements from Pb to Fm. With such estimates, however, one should be careful since they contain a lot of uncertainties. Nevertheless, the FaNDF$^0$ prediction for the drip line seems to be in the line with typical Skyrme EDFs.
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References

[1] D. Vautherin and D. M. Brink, Phys. Rev. C 5, 626 (1972).
[2] J. Dechargé and D. Gogny, Phys. Rev. C 21, 1568 (1980).
[3] P. Ring, Prog. Part. Nucl. Phys. 37, 193 (1996).
[4] W. Kohn and L. J. Sham, Phys. Rev. 140, A1133 (1965).
[5] P. Hohenberg and W. Kohn, Phys. Rev. 136, B864 (1964).
[6] J. Bartel, P. Quentin, M. Brack, C. Guet, and H. B. Häkansson, Nucl. Phys. A 386, 79 (1982).
[7] E. Chabanat, P. Bonche, P. Haensel, J. Meyer, and R. Schaeffer, Nucl. Phys. A 635, 231 (1998).
[8] M. Bender, P.-H. Heenen, and P.-G. Reinhard, Rev. Mod. Phys. 75, 121 (2003).
[9] S. Goriely, N. Chamel, and J. M. Pearson, Phys. Rev. Lett. 102, 152503 (2009).
[10] S. Goriely, [http://www-astro.ulb.ac.be/brushlib/nudata/](http://www-astro.ulb.ac.be/brushlib/nudata/)
[11] M. Kortelainen, J. McDonnell, W. Nazarewicz, P.-G. Reinhard, J. Sarich J, N. Schunck, M. V. Stoitsov, and S. M. Wild, Phys. Rev. C 85, 024304 (2012).
[12] M. Baldo, P. Schuck, and X. Viñas, Phys. Lett. B 663, 390 (2008).
[13] M. Baldo, L. M. Robledo, P. Schuck, and X. Viñas, Phys. Rev. C 87, 064305 (2013).
[14] A. V. Smirnov, S. V. Tolokonnikov, and S. A. Fayans, Sov. J. Nucl. Phys. 48, 995 (1988).
[15] I. N. Borzov, S. A. Fayans, E. Kromer, and D. Zawischa, Z. Phys. A 355, 117 (1996).
[16] S. A. Fayans, JETP Lett. 68, 169 (1998).
[17] S. A. Fayans, S. V. Tolokonnikov, E. L. Trykov, and D. Zawischa, Nucl. Phys. A 676, 49 (2000).
[18] V. A. Khodel, E. E. Saperstein, Phys. Rep. 92, 183 (1982).
[19] A. B. Migdal, *Theory of finite Fermi systems and applications to atomic nuclei* (Nauka, Moscow, 1965; transl. Wiley, New York, 1967).
[20] S. A. Fayans and V. A. Khodel JETP Lett. 17, 444 (1973).
[21] I. N. Borzov, E. E. Saperstein, and S. V. Tolokonnikov, Phys. At. Nucl. 71, 469 (2008).
[22] I. N. Borzov, E. E. Saperstein, S. V. Tolokonnikov, G. Neyens, and N. Severijns, Eur. Phys. J. A 45, 159 (2010).
[23] S. V. Tolokonnikov, S. Kamerdzhiev, S. Krewald, E. E. Saperstein, and D. Voitenkov, Eur. Phys. J. A 48, 70 (2012).
[24] S. Kamerdzhiev, S. Krewald, S. Tolokonnikov, E. E. Saperstein, and D. Voitenkov, EPJ Web of Conferences 38, 10002 (2012).
[25] E. E. Saperstein, S. V. Tolokonnikov, Phys. At. Nucl. 74, 1277 (2011).
[26] I. N. Borzov, Phys. Rev. C 67, 025802 (2003); Phys. Rev. C 71, 065801 (2005).
[27] S. V. Tolokonnikov, S. Kamerdzhiev, D. Voytenkov, S. Krewald, and E. E. Saperstein, Phys. Rev. C 84, 064324 (2011).
[28] S. V. Tolokonnikov, S. Kamerdzhiev, S. Krewald, E. E. Saperstein and D. Voitenkov, Eur. Phys. J. Web of Conferences 38, 04002 (2012).
[29] N. V. Gnezdilov, I. N. Borzov, E. E. Saperstein, and S. V. Tolokonnikov, Phys. Rev. C 89, 034304 (2014).
[30] S. V. Tolokonnikov and E. E. Saperstein, Phys. At. Nucl. 73, 1684 (2010).
[31] S. V. Tolokonnikov, I. N. Borzov, M. Kortelainen, Yu. S. Lutostansky, and E. E. Saperstein, J. Phys. G 42, 075102 (2015).
[32] M. V. Stoitsov, N. Schunck, M. Kortelainen, N. Michel, H. Nam, E. Olsen, J. Sarich, and S. Wild, Comp. Phys. Comm. 184, 1592 (2013).
[33] J. Erler, N. Birge, M. Kortelainen, W. Nazarewicz, E. Olsen, A. M. Perhac, and M. Stoitsov, Nature 486, 509 (2012).
[34] A. V. Afanasjev, S. E. Agbemava, D. Ray, and P. Ring, Phys. Rev. C 91, 014324 (2015).
[35] T. Kajino, S. Wanajo, and G. J. Mathews, Nucl. Phys. A, 784, 165 (2002).
[36] I. V. Panov, Astron. Lett. 29, 163 (2003).
[37] I. Petermann, K. Langanke, G. Martinez-Pinedo, I. V. Panov, P.-G. Reinhard, and F.-K. Thielemann, EPJ A, 48, 122 (2012).
[38] M. Kortelainen, J. Phys. G 42, 034021 (2015).
[39] M. Baldo, U. Lombardo, E. E. Saperstein, and M. V. Zverev, Phys. Lett. B 533, 17 (2002).
[40] E. E. Saperstein and S. V. Tolokonnikov, JETP Lett. 78, 343 (2003).
[41] G. Audi, A. H. Wapstra, and C. Thibault, Nucl. Phys. A 729, 337 (2003).
[42] J. Terasaki, J. Engel, and G. F. Bertsch, Phys. Rev. C 78, 044311 (2008).