Spectral modeling of type II supernovae

II. A machine-learning approach to quantitative spectroscopic analysis

C. Vogl\textsuperscript{1,2}, W. E. Kerzendorf\textsuperscript{3,4,5}, S. A. Sin\textsuperscript{6}, U. M. Noebauer\textsuperscript{1,7}, S. Lietzau\textsuperscript{1,8}, and W. Hillebrandt\textsuperscript{1}

\textsuperscript{1} Max-Planck-Institut für Astrophysik, Karl-Schwarzschild-Str. 1, 85741 Garching, Germany
e-mail: cvogl@mpa-garching.mpg.de
\textsuperscript{2} Physik Department, Technische Universität München, James-Franck-Str. 1, 85741 Garching, Germany
\textsuperscript{3} Center for Cosmology and Particle Physics, New York University, 726 Broadway, New York, NY 10003, USA
\textsuperscript{4} Department of Physics and Astronomy, Michigan State University, East Lansing, MI 48824, USA
\textsuperscript{5} Department of Computational Mathematics, Science, and Engineering, Michigan State University, East Lansing, MI 48824, USA
\textsuperscript{6} Astrophysics Research Centre, School of Mathematics and Physics, Queen’s University Belfast, Belfast BT7 1NN, UK
\textsuperscript{7} MunichRe IT 1.6.1.1, Königstraße 107, 80802 Munich, Germany
\textsuperscript{8} Vector Informatik GmbH - Niederlassung München, Baierbrunnerstraße 23, 81379 Munich, Germany

Received 19 June 2019 / Accepted 12 November 2019

ABSTRACT

There are now hundreds of publicly available supernova spectral time series. Radiative transfer modeling of this data provides insight into the physical properties of these explosions, such as the composition, the density structure, and the intrinsic luminosity, which is invaluable for understanding the supernova progenitors, the explosion mechanism, and for constraining the supernova distance. However, a detailed parameter study of the available data has been out of reach due to the high dimensionality of the problem coupled with the still significant computational expense. We tackle this issue through the use of machine-learning emulators, which are algorithms for high-dimensional interpolation. These use a pre-calculated training dataset to mimic the output of a complex code but with run times that are orders of magnitude shorter. We present the application of such an emulator to synthetic type II supernova spectra generated with the TARDIS radiative transfer code. The results show that with a relatively small training set of 780 spectra we can generate emulated spectra with interpolation uncertainties of less than one percent. We demonstrate the utility of this method by automatic spectral fitting of two well-known type II supernovae; as an exemplary application, we determine the supernova distances from the spectral fits using the tailored-expanding-photosphere method. We compare our results to previous studies and find good agreement. This suggests that emulation of TARDIS spectra can likely be used to perform automatic and detailed analysis of many transient classes putting the analysis of large data repositories within reach.

Key words. radiative transfer – methods: numerical – methods: statistical – supernovae: general – supernovae: individual: 1999em – supernovae: individual: 2005cs

1. Introduction

In recent years, improvements in instrumentation as well as the supply of targets have led to a tremendous increase in the volume of spectral data gathered for astrophysical transients of all kinds. At the same time, public databases such as the WISEREP\textsuperscript{1} archive (Yaron & Gal-Yam 2012) or the Open Supernova Catalog\textsuperscript{2} (Guillochon et al. 2017) have made access to this data easier than ever before; WISEREP alone provides 35484 spectra for 10809 transients\textsuperscript{3}.

In contrast, our tools for analyzing these large spectral datasets have lagged behind. We can distinguish between two sets of approaches for dealing with such numbers of spectra. The most prevalent approach is to break the spectra down to a few easily measurable diagnostic properties (e.g., line absorption velocities, equivalent widths), which are then studied for correlations (e.g., Gutiérrez et al. 2017, among many). The second approach is to use the spectra as input for machine-learning techniques; exemplary applications include spectroscopic classification (e.g., Yip et al. 2004) or the detection of sub-classes, for example of type Ia supernovae (Sasdelli et al. 2016). These approaches provide information about the specific measured quantities but do not provide a whole picture of the transient. Radiative transfer models have the power to infer underlying physical properties such as the composition and structure of the ejecta; we constrain these quantities by adjusting parametrized models of the emitting objects such that the simulated and observed spectra match. This provides, for example, information about the progenitor systems of the explosion for many kinds of transients (e.g., Hachinger et al. 2012 for SN Ic, Barna et al. 2017 for SN Iax). The main obstacle is the high cost of radiative transfer simulations; depending on the complexity of the underlying code, the time needed to calculate a single synthetic spectrum ranges between minutes and days. This is exacerbated by high-dimensional parameter spaces; we usually aim to determine a combination of various abundances, the density profile, photospheric temperatures, and velocities (e.g., Dessart & Hillier 2006; Baron et al. 2007). It is prohibitively expensive to explore this parameter space automatically with radiative transfer models, which would be needed to identify the parameters that best reproduce the observed spectrum; instead, the current standard method is to optimize the agreement by hand, relying heavily on the expertise of the modeler (e.g.,...
These models, we assume the ejecta to be spherically symmetric to make inferences about the supernova properties. In defining steps.

One way to overcome the large computational expense of radiative transfer models in spectral fitting is to devise a fast algorithm that mimics the code. A very simple implementation of such an algorithm is interpolation in a pre-computed Cartesian grid. However, high-dimensional problems such as supernovae require the use of more complex algorithms known as emulators. In essence, the emulator learns the mapping from the simulation input to the output from a set of examples; the simulator, in this context, is treated as a black box. Emulators are used extensively, for example in engineering, but have not yet found widespread application in astrophysics. Some of the sparse cases have been the prediction of the nonlinear matter power spectrum (Heitmann et al. 2009), stellar spectra (Czekala et al. 2015), and type Ia supernova spectra (Lietzau 2017). In this paper, we apply emulation to perform automated quantitative spectroscopic analysis of type II supernovae (SNe II). We use Gaussian-process interpolation in the principal component analysis (PCA) space to reproduce the output of our radiative transfer code, a modified version of the Monte Carlo (MC) code TARDIS (Vogl et al. 2019). With the emulator, we reduce the time for the calculation of a synthetic spectrum from hours to milliseconds; this in turn makes it possible to fit spectra using conventional optimization methods or to explore the parameter space with a sampler.

We showcase the emulator by inferring distances to type IIP supernovae using the tailored-expanding-photosphere method (tailored EPM; Dessart & Hillier 2006; Dessart et al. 2008). This method uses spectroscopic analysis of type IIP supernovae to obtain distances with small uncertainties, for example for cosmological studies. A cosmological application requires a large number of uniformly studied supernovae, which will be made possible by the use of emulators. Such an endeavor will provide an independent, physics-based probe of the cosmic expansion history.

Section 2 provides a short introduction to supernova models and their use for parameter inference. Section 3 describes the library of synthetic spectra that forms the basis of our machine-learning approach. Section 4 is dedicated to the presentation of the spectral emulator: the machine-learning techniques, the training process, and the prediction step. In Sect. 5, we assess the predictive performance by comparing emulated and simulated spectra for a set of independent test models. We continue with the application of the emulator to the modeling of spectra of SN 1999em and SN 2005cs in Sect. 7. We show the application of measuring distances using the tailored EPM in Sect. 7.3. Section 8 summarizes the results and gives an outlook on future steps.

2. Parametrized supernova models with TARDIS

We use simple parametrized models of the supernova ejecta to make inferences about the supernova properties. In defining these models, we assume the ejecta to be spherically symmetric and in homologous expansion. This allows us to discretize the spectrum formation region into a set of shells that are specified by their composition, density, and expansion velocity. It is often useful to simplify the model specification further, for example by assuming an analytic form for the density profile (e.g., a power law) or by assuming uniform abundances – this reduces the number of parameters considerably.

Since we do not simulate the creation of the radiation field self-consistently, we treat the radiation field at the inner boundary as a model parameter. Specifically, we assume a blackbody characterized by a temperature $T_{\text{inner}}$; this is well motivated for SNe II since the continuum opacity from hydrogen leads to a full thermalization of the radiation field at high optical depths.

To assess if the thus-defined parametrized model is consistent with observations, we simulate the radiation transport through the discretized ejecta and then compare the synthetic and observed spectra. In TARDIS (Kerzendorf & Sim 2014), we use a Monte Carlo approach based on the indivisible energy packet scheme of Lucy (1999a,b, 2002, 2003) to this end. The version used in this paper (Vogl et al. 2019) simulates the effects of bound-bound, bound-free, free-free, as well as collisional interactions on the radiation field; it accounts for NLTE effects in the excitation and ionization of hydrogen and calculates the thermal structure of the envelope from the balance of heating and cooling processes.

3. Creation of a SN II spectral training set

As a first step towards the spectral emulator, we need to calculate a set of synthetic SNe II spectra, which will serve as the training data. We selected photospheric velocity $v_{\text{ph}}$, photospheric temperature $T_{\text{ph}}$, metallicity $Z$, time of explosion $t_{\exp}$, and steepness of the density profile $n = -\frac{\ln\rho}{\ln r}$ as the parameters of our model grid. The latter provides a simple parametrization of the density profile, which, as demonstrated for example by Chevalier (1976), Blinnikov et al. (2000), and Dessart & Hillier (2006), describes the outer density distribution with sufficient accuracy.

Most of the spectral evolution of photospheric phase SNe II, as well as the differences between individual objects, can be explained by variations in the expansion velocity, the temperature, and the density profile. As such, the parameters usually considered in quantitative spectroscopic analyses, such as those of Dessart & Hillier (2006) or Dessart et al. (2008) are $v_{\text{ph}}, T_{\text{ph}},$ and $n$. In addition to these essential parameters, we include the metallicity $Z$. Observed SNe II show a wide range of metallicities (see e.g., Anderson et al. 2016; Taddia et al. 2016) and the associated changes to the spectrum are significant, in particular in the blue. For the purpose of inferring accurate distances, it is also important to allow for variations in the time of explosion $t_{\exp}$. While the effects on the shape of the spectral energy distribution (SED) are small, $t_{\exp}$ affects the absolute value of the flux through the modulation of the photospheric density (for any given density profile) and therefore the amount of continuum flux dilution (see e.g., Eastman et al. 1996). Other potentially relevant parameters are the abundances of CNO process elements, which have been investigated for example by Baron et al. (2007), as well as the H/He abundance ratio as studied for example by Dessart & Hillier (2006). For the first

---

4 https://doi.org/10.5281/zenodo.1312512
5 See Sect. 4.1 for more details on PCA.
6 We define the photospheric temperature $T_{\text{ph}}$ as the temperature of the electron gas at an electron scattering optical depth of $\tau = 2/3$.
7 We use metallicity to refer to the abundances of all elements except He, C, N, and O. The mass fractions of the thus-defined metal species are multiples of the solar neighborhood values $Z_\odot$ of Asplund et al. (2009).
Table 1. Parameter range covered by the spectral library.

| $v_{\text{ph}}$ [km s$^{-1}$] | $T_{\text{ph}}$ [K] | $Z$ [Z$_\odot$] | $t_{\text{exp}}$ [days] | $n$ |
|-----------------------------|-------------------|-----------------|----------------------|-----|
| Min                         | 3700              | 0.1             | 6.5                  | 6   |
| Max                         | 10 500            | 3.0             | 22.0                 | 16  |

Specifically, we adopt the following number density ratios: $8 \times 10^{-3}$, $C/\text{He} = 1.7 \times 10^{-4}$, and $O/\text{He} = 10^{-3}$. These ratios together with the mass fractions of the metal species specify the composition completely. Typically, the inner edge of our computational domain, where the packets are injected, lies at an electron scattering optical depth of around 20.

demonstration of our method, we refrain from varying these parameters and instead adopt CNO-cycle equilibrium values for the relevant abundances from Prantzos et al. (1986) as in Dessart & Hillier (2005, 2006)$^8$.

Table 1 lists the ranges of parameters $v_{\text{ph}}$, $T_{\text{ph}}$, $Z$, $t_{\text{exp}}$, and $n$ covered by our model grid. We have chosen the parameter space such that it allows for the modeling of a large variety of SNe II between roughly one and three weeks after explosion.

In practice, we cannot directly specify $T_{\text{ph}}$ and $v_{\text{ph}}$ since both are emergent and not input properties of the simulation; instead, we use the inner boundary temperature $T_{\text{inner}}$, that is to say the temperature of the injected blackbody radiation$^9$, and a simple analytic estimate for the photospheric velocity $v_{\text{ph}}$. We set up a five-dimensional latin hypercube design (Stein 1987) in these parameters, which is optimized to fill the space nearly uniformly. In the next step, we perform radiative transfer calculations for the resulting set of 780 models and obtain synthetic spectra as well as the real values of $T_{\text{ph}}$ and $v_{\text{ph}}$. Figure 1 shows pairwise projections for the completed set of parameters $v_{\text{ph}}$, $T_{\text{ph}}$, $Z$, $t_{\text{exp}}$, and $n$. The grid of models displays a slight distortion in the $v_{\text{ph}}$-$T_{\text{ph}}$ plane as a result of our use of $v_{\text{ph}}$ and $T_{\text{inner}}$ as proxies for these quantities.

A common approach in machine learning is to generate a test set in addition to the training set to assess the predictive accuracy. We compute 225 models (in addition to the 780 training models). The parameters for these models are sampled uniformly from the same range of $v_{\text{ph}}$, $T_{\text{inner}}$, $Z$, $t_{\text{exp}}$, and $n$ as covered by the training data. We include the properties of the test data in Fig. 1 to facilitate the comparison between the sets of models.

One of the challenges in the setup of the model grid is deciding how large the training set of models really needs to be. Ideally, the number of training models should be large enough to guarantee that the interpolation uncertainty in the spectra is not the dominant contribution to the error in the inferred parameters; at the same time, the training size should be kept as small as possible for reasons of computational expediency. In practice, the best possible trade-off is difficult to identify since the conversion from the interpolation errors in the spectra to errors in the parameters is nontrivial. To be on the safe side however one can aim to have the interpolation uncertainty significantly smaller than the systematic mismatch between model and observation; for the parameter space we consider, this is indeed the case for the training set we used (see Sect. 5).

4. Spectral emulator

We use the synthetic spectra from the previous section to create two separate emulators: one for spectra and one for absolute magnitudes. We set up these emulators in two steps. First, we preprocess the training data and synthesize absolute magnitudes; this is followed by dimensionality reduction of the preprocessed spectra through PCA decomposition. Second, we train Gaussian processes to interpolate the spectra within the PCA space and to predict absolute magnitudes.

4.1. Preprocessing and dimensionality reduction

The synthetic spectra have a range of values that varies widely both with wavelength and between models. In addition, they contain non-negligible Monte Carlo noise. For the successful application of machine-learning techniques, it is crucial to preprocess the noisy, unscaled data to standardize them and to remove unwanted sources of variation. We start by smoothing the spectra with a fifth-order Savitzky-Golay filter (Savitzky & Golay 1964) to reduce the effect of Monte Carlo noise. Savitzky-Golay filtering performs well in preserving the shape of spectral features, even weak ones, which makes it a popular choice for denoising astrophysical spectra (see e.g., Hügelmeyer et al. 2007; Pozzanski et al. 2010; Sasdelli et al. 2015). Next, we approximately correct for the redshifts in the position of spectral features between models by Doppler shifting each spectrum by the photospheric velocity $v_{\text{ph}}$. This roughly maps the absorption minimum of a spectral feature to the same wavelength for all models. Since we do not assume a distance for fitting an observed spectrum (see Sect. 7), we can standardize the spectral library further by discarding the information about the luminosity. Specifically, we normalize the shifted synthetic spectra to have unit flux at 6000 Å; this provides a good standardization of the continuum flux levels between models since no strong line features form at this position. Finally, we apply a linear transformation to the fluxes in each wavelength bin such that in each bin the values for the full spectral library span a range from −0.5 to 0.5 (see Appendix A). For each preprocessing step, we restrict the considered wavelength range to the minimum range needed to model the observations in Sect. 7$^10$. In practice, this corresponds to a wavelength window from roughly 3200 Å to 9500 Å. In contrast, we only smooth the test spectra but do not preprocess them further: we compare them to the emulated spectra in the same fashion as for observational data.

In the final step, we reduce the dimensionality of our spectral library. Each preprocessed spectrum consists of a few thousand wavelength bins, a number which by far exceeds that of the physical parameters used in its creation. To obtain a less correlated, more compact representation of our data, we use PCA$^{11}$. Principal component analysis has been applied successfully to observed spectra of a wide range of astrophysical objects, including quasars (e.g., Francis et al. 1992), stars (e.g., Bailey-Jones et al. 1998), galaxies (e.g., Connolly et al. 1995), and supernovae (e.g., Sasdelli et al. 2015; Williamson et al. 2019). The basic idea is to find an orthogonal basis for the data that is a linear transformation of the original but where the axes are aligned with the directions of maximal variance. Since by construction each successive principal component explains less of the variance in the data, we can reduce the dimensionality of our dataset by truncating the basis; instead of using the full set of $N_L$ principal component eigenvectors, where $N_L$ is the number of wavelengths, we use only $N_L$ eigenvectors whose cumulative variance exceeds a threshold.

$^8$ Specifically, we adopt the following number density ratios: $H/\text{He} = 5$, $\text{N}/\text{He} = 6.8 \times 10^{-3}$, $\text{C}/\text{He} = 1.7 \times 10^{-4}$, and $\text{O}/\text{He} = 10^{-3}$. These ratios together with the mass fractions of the metal species specify the composition completely.

$^9$ Typically, the inner edge of our computational domain, where the packets are injected, lies at an electron scattering optical depth of around 20.

$^{10}$ We note that this wavelength range deviates slightly from that of the observed spectra to allow for Doppler shifting the model spectra in the preprocessing.

$^{11}$ Specifically, we use the probabilistic PCA model of Tipping & Bishop (1999) as implemented in scikit-learn (Pedregosa et al. 2011).
number of spectra in the spectral library, we use only the first $N < N_L$ components. We select the dimensionality $N$ of the truncated basis through cross-validation on the training sample since our main goal is the accurate prediction of synthetic spectra. The cross-validation performance increases at first as more principal components are included but at some point levels off when the additional components stop providing meaningful information; it is at this point that we truncate the PCA basis. For the spectral emulator presented in this paper, this approach leads us to use $N = 80$ principal components, which explain 99.97% of the total variance; this is a significant reduction compared to the original approximately 1500 wavelength bins. If necessary\footnote{For example, for sampling in high-dimensional parameter spaces the emulation speed may become a limitation.}, the number of principal components can be reduced even further with only minor losses in accuracy. By projecting each preprocessed spectrum $\hat{f}_k$ onto the basis vectors $\xi_i$ of the thus-truncated basis, we obtain a compact representation of the input data in terms of a set of $N$ principal component weights $[w_{ik}]$. From these principal component weights, we can reconstruct every input spectrum as a linear combination of the principal components $\xi_i$ and the mean spectrum $\xi_\mu = \sum_k \hat{f}_k / N_L$:

$$\hat{f}_k \approx \xi_\mu + \sum_{i=1}^N w_{ik} \xi_i.$$  \hfill (1)

For the selected number of principal components, the mean fractional reconstruction error for this procedure is 0.26%.

In addition to the spectral preprocessing and the dimensionality reduction, we synthesize Johnson-Cousins $B, V, I$...
4.2. Gaussian process interpolation

4.2.1. Spectra

To predict a spectrum for a new set of input parameters \( \theta = (v_{\text{ph}}, T_{\text{ph}}, Z, n, t_{\text{exp}}) \), we have to interpolate between the principal component weights \( \{w_i\} \), which form the compressed version of our spectral library. We choose to model the weights \( w_i \) for each principal component \( \xi_i \) independently since by construction the weights for the different components are at least linearly uncorrelated. As in Czekala et al. (2015), we use Gaussian processes (GPs; e.g., Rasmussen & Williams 2006) for the interpolation. Gaussian processes are a powerful probabilistic tool for regression analysis, which are steadily gaining in popularity in the astrophysical community (see, e.g., Rajpaul et al. 2015; Foreman-Mackey et al. 2017). As a nonparametric method, GPs offer increased flexibility for modeling complicated signals compared to more conventional approaches such as linear or polynomial regression.

Fundamentally speaking, GPs provide a generalization of the Gaussian probability distribution from finite-dimensional random variables to functions. Following this analogy, each GP is characterized by a mean- and a covariance function. The covariance function \( k \) controls the covariance between the distribution of random function values at any two points \( \theta, \theta' \) in the parameter space. As such, it determines the properties of the functions that can be drawn from the GP, including for example their smoothness, periodicity, and so forth. In the context of regression analysis, the choice of the covariance function sets the prior distribution of functions that we expect to see in the data. A particularly important class of covariance functions are the so-called stationary covariance functions, which do not depend on the positions \( \theta, \theta' \) in the input space but only on their distance \( r = ||\theta - \theta'|| \).

The most commonly used members of this class include the squared exponential, the Matérn, and the rational quadratic covariance function (see, e.g., Rasmussen & Williams 2006; Murphy 2012). The type of covariance function is a hyperparameter of the machine-learning approach and can, similar to the preprocessing steps, be set based on the cross-validation performance. After some experimentation, we adopted covariance functions from the Matérn family:

\[
k_{\text{Matérn}}(r) = \sigma_n^2 \frac{2^{1-v}}{\Gamma(v)} \left( \frac{\sqrt{2}r}{\nu} \right) K_v \left( \frac{\sqrt{2}r}{\nu} \right).
\]

Here, \( \sigma_n^2 \) denotes the signal variance, \( \nu \) is a parameter that regulates the smoothness of the GP, \( \Gamma \) is the gamma function, and \( K_v \) is the modified Bessel function of the second kind. Since we do not expect the weights that encode our MC synthetic smoothness, periodicity, and so forth. In the context of regression analysis, the choice of the covariance function sets the prior distribution of functions that we expect to see in the data.

It is customary to assume a zero mean for the prior distribution of possible regression functions (see, e.g., Rasmussen & Williams 2006).

4.2.2. Absolute magnitudes

In Sect. 4.1, we removed the luminosity information from the synthetic spectra to standardize them further for PCA. We train additional GPs for the prediction of the absolute magnitudes, which we need for our distance inferences in Sect. 7.

As part of the data preprocessing, we synthesized Johnson-Cousins \( S = \{B,V,I\} \) magnitudes \( M_S \) from the unprocessed synthetic spectra. Before we use these as training data for the GPs, we remove the variation in the magnitudes introduced by differences in the physical sizes of the supernova models. Specifically, we transform from absolute magnitudes to magnitudes at the position of the photosphere

\[
m_S^\text{ph} = M_S + 5 \log \frac{R_{\text{ph}}}{10}\text{pc}.
\]
where $R_{\text{ph}} = v_{\text{ph}}/v_{\text{exp}}$. We model each bandpass with a GP with a Matérn covariance function (see, Eq. (2)) that has a smoothness parameter $\nu = 5/2$. The hyperparameters ($\sigma_n^2, \ell_n, \cdots, \ell_{n_{\text{exp}}}$) for the individual bandpasses are set in the same fashion as for the spectral emulator. Finally, to predict absolute magnitudes for a new set of input parameters $\theta = (v_{\text{ph}}, T_{\text{ph}}, Z, n, t_{\text{exp}})$, we evaluate the trained GP and subtract $5 \log(R_{\text{ph}}/10 \text{ pc})$.

5. Evaluation of the emulator performance

To allow the reliable inference of parameters from supernova spectra, it is crucial that the emulator reproduces the output of our simulation code TARDIS to high precision. We assess the predictive performance of our method by comparing the predicted spectra and absolute magnitudes to a set of independently collected test data. Our strategy for the calculation of the 225 test models is described in detail in Sect. 3 and the associated preprocessing procedure in Sect. 4.1.

5.1. Spectra

In Fig. 2, we compare simulated and emulated spectra for a subset of the test models; the selected subset approximately spans the range of deviations encountered in the full test data. We scaled the emulated spectra back to physical units for the comparison of spectral shapes. Despite covering a wide variety of spectral appearances, including for example SEDs with very broad or very narrow features, with or without line blanketing, the agreement is excellent overall. In addition, in most cases, the deviations are within the 95% confidence interval of the emulator prediction with areas of larger residuals corresponding to regions with increased emulation uncertainties.

In order to quantify the test performance, we need to define a quality metric that expresses the mismatch between two spectra in a single number. We use the mean fractional error (MFE)

$$\text{MFE} = \frac{1}{N_i \lambda} \sum_{i=1}^{N_i} \frac{|f^{\text{emu}}_{i,\lambda} - f^{\text{test}}_{i,\lambda}|}{f^{\text{test}}_{i,\lambda}},$$

where $f^{\text{test}}_{i,\lambda}$ and $f^{\text{emu}}_{i,\lambda}$ are the test and emulated spectra respectively, and $N_i$ is the number of wavelength bins. By using the MFE instead of for example the mean squared error, we give the mean of principal components fixed, thus starting with a minimum training size of 80. In the investigated regime, the mean error on the training set is almost constant at around 0.5%. At least part of this error can plausibly be attributed to the MC noise inherent to the models. From the small training errors, we conclude that our model does not suffer from high bias, that is to say, the model is flexible enough to provide a satisfactory fit to the training data. The mean test error decreases steadily from its initial value of 1.7% as the number of training instances is increased and quickly drops below 1%. Finally, for the maximum training size, a test score of 0.7% is reached. At this point, the difference between training and test score is small but non-negligible. The gap between the scores will be reduced even further as more training instances are added since the test score is still decreasing (albeit at a slower rate). We conclude that our model generalizes well and does not overfit the training data.

5.2. Absolute magnitudes

For the purpose of measuring accurate distances, it is crucial that we can accurately predict the luminosity for any combination of input parameters. We assess the accuracy of our approach by comparing the synthetic photometry of the test models to the absolute magnitudes predicted by the emulator. As shown in Fig. 4, the median difference between the predicted and true magnitudes is less than 0.0012 mag; this confirms that the emulator provides an unbiased estimate of the true model luminosity. The accuracy of the predictions decreases from the redder to the bluer parts of the spectrum. We summarize the test performance for the absolute magnitudes as a function of the number of models used for training, for both the test and the training sample. We keep the number of principal components fixed, thus starting with a minimum training size, a test score of 0.7% is reached. At this point, the difference between training and test score is small but non-negligible. The gap between the scores will be reduced even further as more training instances are added since the test score is still decreasing (albeit at a slower rate). We conclude that our model generalizes well and does not overfit the training data.

Finally, we compare the emulator to the often used approach of simply picking the best-fitting model from the grid. We start by creating a learning curve for the spectral emulator as shown in Fig. 6. The learning curve shows the accuracy of the emulator as a function of the number of models used for training, for both the test and the training sample. We keep the number of principal components fixed, thus starting with a minimum training size of 80. In the investigated regime, the mean error on the training set is almost constant at around 0.5%. At least part of this error can plausibly be attributed to the MC noise inherent to the models. From the small training errors, we conclude that our model does not suffer from high bias, that is to say, the model is flexible enough to provide a satisfactory fit to the training data. The mean test error decreases steadily from its initial value of 1.7% as the number of training instances is increased and quickly drops below 1%. Finally, for the maximum training size, a test score of 0.7% is reached. At this point, the difference between training and test score is small but non-negligible. The gap between the scores will be reduced even further as more training instances are added since the test score is still decreasing (albeit at a slower rate). We conclude that our model generalizes well and does not overfit the training data.

6. Learning behavior of the emulator

In this section, we address questions about the number of models needed for a desired accuracy, the adequacy of the adopted methods, and how the emulator compares to the standard approach of picking the best-fitting model from the grid.

We start by creating a learning curve for the spectral emulator as shown in Fig. 6. The learning curve shows the accuracy of the emulator as a function of the number of models used for training, for both the test and the training sample. We keep the number of principal components fixed, thus starting with a minimum training size of 80. In the investigated regime, the mean error on the training set is almost constant at around 0.5%. At least part of this error can plausibly be attributed to the MC noise inherent to the models. From the small training errors, we conclude that our model does not suffer from high bias, that is to say, the model is flexible enough to provide a satisfactory fit to the training data. The mean test error decreases steadily from its initial value of 1.7% as the number of training instances is increased and quickly drops below 1%. Finally, for the maximum training size, a test score of 0.7% is reached. At this point, the difference between training and test score is small but non-negligible. The gap between the scores will be reduced even further as more training instances are added since the test score is still decreasing (albeit at a slower rate). We conclude that our model generalizes well and does not overfit the training data.

Finally, we compare the emulator to the often used approach of simply picking the best-fitting model from the grid. Figure 7 shows the test scores for both approaches as a function of the number of training instances; the plot highlights the massive reduction in the number of models that are needed to achieve a given precision. The emulator with the minimum considered training size of 80 outperforms the method of picking the near-

15 As discussed in Sect. 4.1, we discard any useful luminosity information during the preprocessing of the training spectra; this means that it is only meaningful to compare spectral shapes.

16 The MC noise manifests itself not only as Poisson noise in the synthetic spectra but also in terms of complicated correlated noise that arises from the MC uncertainties in the plasma state quantities.
Fig. 2. Evaluation of the emulator performance. The test performance is summarized in the top left panel, which shows a histogram of the test errors; specifically, the MFE (see Eq. (7)) is displayed. The other panels provide a direct comparison between emulated and simulated spectra for a subset of the test data. Each panel contains a histogram of the test errors, in which the position of the current model is highlighted. To highlight the subtle differences between the predicted and true spectra, the fractional difference $\Delta L/L$ is shown in the lower section of each panel (solid blue line). In both sections, the shaded regions indicate the 68% and 95% confidence intervals for the prediction of the emulator.
Fig. 3. Test errors for the spectral emulator as a function of the input parameters. We show the color-coded MFE (see Eq. (7)) between emulated and simulated spectra for all two-dimensional projections of the test parameters. The region enclosed by the dashed black line indicates the parameter space covered by the training data.

We found that the training model even when the full set of 780 spectra is used. To get a rough estimate of how many models would be needed to match the final accuracy of 0.7% of the emulator, we linearly extrapolate the learning curve in log-linear space; this yields on the order of 15 000 spectra. This is a conservative lower limit for the number of needed models since it generously assumes a constant learning rate.

7. Modeling observations

With the spectral emulator, we can fit SN II spectral time series in an automated fashion. For a first demonstration, we select SN 1999em and SN 2005cs as our test objects. SN 1999em is considered by many to be the prototype of a type II supernova, whereas SN 2005cs is a more peculiar, subluminous object. Both are among the best-observed type II supernovae, with extensive datasets including photometry and spectroscopy at UV, optical, and infrared wavelengths (Leonard et al. 2001, 2002; Hamuy et al. 2001; Dessart & Hillier 2006; Pastorello et al. 2006, 2009; Tsvetkov et al. 2006; Bufano et al. 2009). Both SNe have been studied with detailed NLTE radiative transfer models using CMFGEN (Dessart & Hillier 2006; Dessart et al. 2008) and PHOENIX (Baron et al. 2004, 2007). Here we compare the results of our automated fits to these analyses, which have been conducted carefully by hand. In our comparison, we focus on the studies of Dessart & Hillier (2006) and Dessart et al. (2008), which model more epochs and have published the relevant inferred parameters, namely $T_{ph}$, $v_{ph}$ and $n$. In the final step, we
infer distances to the supernovae from our fits using the tailored-expanding-photosphere method.

7.1. Likelihood for parameter inference

We use a standard multi-dimensional Gaussian likelihood function for parameter inference. In this case, the log-likelihood of an observed spectrum $f_{\lambda}^{\text{obs}}$ with $N_{\text{pix}}$ spectral bins is given by

$$\ln p(f_{\lambda}^{\text{obs}} | \theta_{\text{SN}}, E(B - V)) = -\frac{1}{2} \left( R^T C^{-1} R + \ln \det C + N_{\text{pix}} \ln 2\pi \right),$$

where

$$R = f_{\lambda}^{\text{obs}} - f_{\lambda}(\theta_{\text{SN}}, E(B - V)),$$

are the residuals with respect to the emulated, reddened spectrum $f_{\lambda}$ and $C$ is the pixel-by-pixel covariance matrix (e.g., Czekala et al. 2015). As before, $\theta_{\text{SN}} = (v_{\phi}, T_{\phi}, Z, n, t_{\text{exp}})$ are the parameters of our SN model and $E(B - V)$ is the color excess\(^{17}\). The residuals have pixel-to-pixel correlations mostly due to imperfections in the model calculations (see Czekala et al. 2015). For example, a slight error in the ionization balance of a given element will lead to features in the synthetic spectrum that are either systematically too weak or too strong, producing highly correlated residuals in these regions. If these correlations are not accounted for in the covariance matrix $C$, the uncertainties of the inferred parameters will be severely underestimated (Czekala et al. 2015). We find typical uncertainties for the photospheric temperature of the order of a few Kelvin if we only

\(^{17}\) We assume a ratio of total to selective absorption of $R_V = 3.1$ as appropriate for Milky Way-type dust.
include the interpolation uncertainty and the photon count noise; thus, without a good statistical model for the correlated residuals, the inferred uncertainties are essentially meaningless. For the purpose of a first demonstration, we resort to a simple maximum-likelihood approach with homoscedastic white noise, that is to say a diagonal, constant covariance matrix. Our rationale for using homoscedastic white noise instead of a combination of the heteroscedastic photon noise and the interpolation uncertainties is that the systematic mismatches between model and observation are the dominant error component in most regions; ignoring these mismatches means that we assign highly variable and essentially meaningless weights to different parts of the spectrum.

7.2. Fitting observed spectra

We want to compare our framework for parameter inference to the quantitative spectroscopic analyses of Dessart & Hillier (2006) and Dessart et al. (2008) – detailed NLTE studies conducted carefully by hand by experts. To allow an unbiased comparison of the inferred parameters, we copy key assumptions of these studies. First, we adopt solar metallicities for the non-CNO processed elements. Second, we use the same elapsed times since explosion as utilized in the calculation of their spectral models; this is particularly important for the comparison of photospheric temperatures, which are sensitive to this parameter. Third, we adopt a color excess of \( E(B-V) = 0.1 \) towards SN 1999em\(^{18} \) and a color excess of \( E(B-V) = 0.04 \) towards SN 2005s in concordance with Dessart & Hillier (2006) and Dessart et al. (2008). We redden the emulated spectra by this color excess according to the Cardelli et al. (1989) law with \( R_V = 3.1 \). Finally, we blueshift the observed spectra by the peculiar velocities of their host galaxies, which we assume to be 770 km s\(^{-1} \) (Leonard et al. 2002; Dessart & Hillier 2006) for SN 1999em and 466 km s\(^{-1} \) (Dessart et al. 2008) for SN 2005s.

A log of the spectra used as well as relevant model parameters such as the time since explosion utilized in the calculation of the spectral models can be found in Table 2.

7.2.1. SN 1999em

We model three epochs of SN 1999em, covering a time span between roughly two and four weeks after explosion. In Fig. 8, we show the maximum likelihood emulated spectra in comparison to the observations, highlighting the good agreement between the two\(^{19} \). For each spectral epoch, a table with the inferred maximum likelihood parameters as well as the literature values from Dessart & Hillier (2006) is attached to the plot. Despite using vastly different methods for calculating synthetic spectra and for adjusting them to match the observations, we find good agreement in the inferred parameters, with maximum differences of only 285 K in photospheric temperature, 351 km s\(^{-1} \) in photospheric velocity, and 0.8 in the steepness of the density profile. We visualize this in Fig. 11, which plots our values for \( v_{\text{ph}} \) and \( T_{\text{exp}} \) against those of Dessart & Hillier (2006). Whereas our best fit parameters for \( T_{\text{ph}} \) and \( v_{\text{ph}} \) fall below or above those of Dessart & Hillier (2006) depending on the epoch, we find systematically higher values for the power law density index \( n \). To investigate this, we examine the influence of the steepness of the density profile on the emergent spectra in Fig. 9 using the epoch of 9 November 1999 as an example. From this, it becomes clear that in the discussed regime of values (density indexes between 10 and 11) the changes in the emergent spectra are small. We see that only strong lines such as H\(_{\alpha} \), which form over a wide range of velocities, are affected at all and even those only slightly.

7.2.2. SN 2005cs

We analyze five closely spaced spectral observations of SN 2005cs, between roughly two and three weeks after explosion. For the first four epochs, there are spectral models from Dessart et al. (2008) at comparable epochs, allowing a comparison of the inferred parameters. The last epoch on 16 July 2005 is used only for our measurement of the distance to the supernova in Sect. 7.3. As for SN 1999em, we show the maximum likelihood emulated spectra combined with tables of the inferred and literature parameters in Fig. 10. Again, we find good agreement in the inferred parameters with only few exceptions.

For the photospheric velocity, the epoch of 14 July 2005 stands out, which shows a deviation of 569 km s\(^{-1} \). In particular, the increase in velocity compared to the previous epoch is puzzling. It can be understood in the following way: as discussed in Sect. 3.3.3 of Dessart & Hillier (2006), spectral fits yield differences on the 10% level in the photospheric velocity depending on which set of lines the fit is optimized on. For the two epochs, our automated fits likely attribute varying weights to certain features, thus giving rise to the inconsistent velocity estimates; for example, on 11 July the Ca infrared triplet absorption is not fit well, forming at overly low velocities, whereas on 14 July the absorption minimum is matched much better.

Regarding photospheric temperature, the earliest epoch has the largest deviation, which is 767 K. We do not know for certain

---

\(^{18}\) This value is slightly higher than our favored reddening of \( E(B-V) = 0.08 \) (see Vogl et al. 2019).

\(^{19}\) Nevertheless, even better agreement between models and observations would be achieved for our favored reddening of \( E(B-V) = 0.08 \) (see Vogl et al. 2019).

---

Table 2. Log of modeled spectra for SN 1999em and SN 2005cs.

| JD (+2 451 474.04) | Date   | Source | \( T_{\text{exp}} \) |
|------------------|--------|--------|-------------------|
| 17.9             | 9 Nov. 1999 | H01   | 9.67              |
| 22.9             | 14 Nov. 1999 | H01   | 11.21             |
| 27.9             | 19 Nov. 1999 | H01   | 22.00\(^{(a)} \) |

| JD (+2 453 549) | Date      | Source | \( T_{\text{exp}} \) |
|-----------------|-----------|--------|-------------------|
| 12.25           | 9 July 2005 | D08   | 14.67             |
| 13.5            | 10 July 2005 | F14   | 16.12             |
| 14.5            | 11 July 2005 | P06   | 15.33             |
| 17.0            | 14 July 2005 | P06   | 16.11             |
| 19.4            | 16 July 2005 | P200  | 19.40             |

Notes. The reference JDs are the estimated times of explosion of Dessart & Hillier (2006) and Pastorello et al. (2009). The abbreviations for the data sources are H01 for Hamuy et al. (2001), P06 for Pastorello et al. (2006), D08 for Dessart et al. (2008), F14 for Faran et al. (2014), and P200 for spectra taken at the Palomar 200-inch Hale Telescope with DBSP. All spectra have been retrieved from the WISEREP archive (Yaron & Gal-Yam 2012). We use the listed time since explosions \( T_{\text{exp}} \), as taken from Dessart & Hillier (2006) and Dessart et al. (2008), for calculating synthetic spectra with the emulator.\(^{(a)}\)As the single exception, we adopt the maximum \( T_{\text{exp}} \) of our spectral emulator for the epoch of the 19 November 1999; this is roughly 19% smaller than the value of \( T_{\text{exp}} = 27.0 \) used by Dessart & Hillier (2006).
Fig. 8. Spectroscopic analysis of SN 1999em. The three subfigures show comparisons between observed (black) and best-fit emulated spectra (blue); the best-fit has been determined through a maximum likelihood approach as outlined in Sect. 7.2. Each spectral comparison is combined with a table of the inferred parameters, the literature values from Dessart & Hillier (2006, D06), and the difference between the two. Since the observations have not been corrected for telluric absorption, we exclude the regions of strongest absorption from the fit (marked ⊙).

Fig. 9. Variation of the spectral shape with the steepness of the density profile $n$. We plot specific flux $f_\lambda$ in arbitrary units for a sequence of emulated spectra where only the power law density index $n$ is modified between spectra; the remaining parameters have been chosen to provide a good fit to SN 1999em for 9 November 1999 (see Fig. 8). We color code the plotted spectra by the power-law density index $n$.

7.3. Distance measurements

In the past, the need to optimize the fit quality by hand and eye combined with the high cost of radiative transfer calculations have made distance measurements from SN II spectral models (e.g., Baron et al. 2004; Dessart & Hillier 2006) a very labor-intensive process. Automated fits based on spectral emulation revise this picture completely.

We use a variant of the tailored EPM (Dessart & Hillier 2006; Dessart et al. 2008) to constrain the distance $D$ to the supernovae. As a first step, we measure the photospheric angular diameter $\Theta = R_{ph}/D = v_{ph}\times t_{exp}/D$ for each epoch. We compare the apparent magnitudes $m_S$ of our best fit model, $m_S = M_S(\theta^*), 5 \log(\Theta) + A_S$, (10) to the observed photometry $m_S^{obs}$ for different values of $\Theta$. Here, $A_S$ is the broadband dust extinction for the bandpass $S = [B,V,I]$ and $M_S(\theta^*)$ is the predicted absolute magnitude for the best-fit parameters $\theta^*$. We adopt the photospheric

---

Footnote: We note that Baron et al. (2007) have invoked similarly steep density distributions at even later epochs (see their radiative transfer model for 31 July 2005).
angular diameter $\Theta^*$ that minimizes the squared difference between observed and model magnitudes:

$$
\Theta^* = \text{arg min}_\Theta \sum_s (m_s - m_s^{\text{obs}})^2.
$$

Our approach to tailored EPM is technically identical to that of Dessart & Hillier (2006) and Dessart et al. (2008) but avoids the detour of parametrizing the model magnitudes by a blackbody color temperature and a dilution factor.

Fig. 10. Spectroscopic analysis of SN 2005cs. See Fig. 8 for a description of the layout. Here, values for the parameter comparison are taken from Dessart et al. (2008, D08). In (e), we only show the inferred parameters since this epoch has not been modeled in Dessart et al. (2008).
Finally, we determine the time of explosion and the distance through a Bayesian linear fit to the time evolution of the ratio of the photospheric angular diameter $\Theta$ and the photospheric velocity $v_{ph}$. To be more specific, we obtain the time of explosion from the intercept with the time axis and the distance from the inverse of the slope. In our analysis, we assume that the uncertainties are Gaussian and that they have standard deviations of 10% of the measured values as in Dessart & Hillier (2006) and Dessart et al. (2008)\textsuperscript{21}. We use a half-Cauchy prior for the slope of the regression curves, corresponding to a uniform distribution for the angle between the straight lines and the time axis. We adopt informative priors for the time of explosion, which we discuss below in the context of the individual supernovae.

Our sources of photometry are Leonard et al. (2002) for SN 1999em (as listed in Table 1 of Dessart & Hillier 2006) and Pastorello et al. (2009) for SN 2005cs. If there is no coincident photometric observation for a given spectral epoch, we linearly interpolate the magnitudes from the nearest epochs. We list all photometric observation for a given spectral epoch, we linearly interpolate the magnitudes from the nearest epochs. We list all magnitudes used in our tailored EPM analysis in Table 3.

### 7.3.1. SN 1999em

For a first demonstration of the emulator, we adopt an informative Gaussian prior for the time of explosion based on the tailored EPM analysis of Dessart & Hillier (2006), which finds $t_0 = JD 2 451 474.04 \pm 1.0$. While the time of explosion for SN 1999em is not well constrained through the photometry, many objects have limits that are as tight or tighter than the adopted prior for $t_0$; this applies, for example, to SN 2005cs as we discuss in the following section.

With the prior for $t_0$ defined, we apply the tailored EPM as outlined above. We summarize the inputs as well as the results of our analysis in Fig. 12. In the figure, we combine a table of the ratios of photospheric angular diameter and velocity $\Theta/v_{ph}$, a visualization of the Bayesian linear regression, and a corner plot of the inferred distance and time of explosion. We find a distance of $11.4^{+1.0}_{-0.9}$ Mpc, which is in excellent agreement with the Cepheid distance to the host galaxy of $11.7 \pm 1$ Mpc (Leonard et al. 2003). It is important to keep in mind that the quoted uncertainties are solely statistical and depend both on the adopted prior for $t_0$ and the assumed uncertainties for $\Theta/v_{ph}$. Finally, we point out that the regression is only weakly informative on the time of explosion, that is to say, the posterior distribution for $t_0$ is only slightly modified compared to the prior.

### 7.3.2. SN 2005cs

As opposed to SN 1999em, the time of explosion for SN 2005cs is constrained tightly by photometric observations. Based on the nondetection at JD = 2 453 548.43 and the detection at JD = 2 453 549.41, Pastorello et al. (2009) identify JD = 2 453 549.0 $\pm$ 0.5 as the time of shock breakout. In our prior for $t_0$, we make small changes to this result to incorporate two basic arguments. First, the prior probability that the first detection is coincident with the explosion should be zero. Secondly, the probability that the explosion occurred before the last nondetection should be non-negligible due to the limited depth of the image. Based on these considerations, we construct the Beta prior shown in Fig. 13. Our prior peaks shortly after the last nondetection and includes the data points from both JD $2 453 549$ and JD $2 453 549.41$.

\begin{table}
\centering
\caption{Interpolated BVI photometry for the epochs of spectral observations.}
\begin{tabular}{llllll}
\hline
SN 1999em & & & & & \\
\hline
JD (+2 451 474.04) & Date & $B$ & $V$ & $I$ \\
\hline
17.9 & 9 Nov. 1999 & 14.02 & 13.84 & 13.48 \\
22.9 & 14 Nov. 1999 & 14.25 & 13.81 & 13.44 \\
27.9 & 19 Nov. 1999 & 14.47 & 13.86 & 13.40 \\
\hline
SN 2005cs & & & & & \\
\hline
JD (+2 453 549) & Date & $B$ & $V$ & $I$ \\
\hline
12.25 & 9 July 2005 & 14.75 & 14.39 & 14.30 \\
13.5 & 10 July 2005 & 14.83 & 14.60 & 14.26 \\
14.5 & 11 July 2005 & 14.92 & 14.58 & 14.25 \\
17.0 & 14 July 2005 & 15.09 & 14.67 & 14.25 \\
19.4 & 16 July 2005 & 15.26 & 14.70 & 14.28 \\
\hline
\end{tabular}
\end{table}

Notes. The reference JDS are the same as in Table 2.

\textsuperscript{21} In the case of a full Bayesian analysis, the assumption of Gaussian uncertainties can be dropped and the posterior distribution of $\Theta/v_{ph}$ can be used instead.
nondetection and has a width that is compatible with the quoted uncertainties of Pastorello et al. (2009). We derive the distance to the supernova as illustrated in Fig. 13 and obtain a value of $7.8^{+0.4}_{-0.3}\text{ Mpc}$.

In contrast to SN 1999em, the distance to SN 2005cs is not constrained through Cepheids. The NASA/IPAC Extragalactic Database (NED)

23 lists 50 individual distance measurements spanning a range of values between 2.45 Mpc and 12.2 Mpc with a median distance of 7.935 Mpc. Based on spectral modeling of SN 2005cs, Dessart et al. (2008) find a distance of $8.9 \pm 0.5\text{ Mpc}$ using tailored EPM in the $BVI$ bandpasses and Baron et al. (2007) $7.9^{+0.3}_{-0.2}\text{ Mpc}$ with the SEAM method. Independent state-of-the-art measurements come from Ciardullo et al. (2002), who derive a distance of $7.6 \pm 0.6\text{ Mpc}$ using the planetary nebula luminosity function (PNLF), and McQuinn et al. (2016), who infer a value of $8.58 \pm 0.10\text{ Mpc}$ from the tip-of-the-red-giant-branch (TRGB) method.

22 The NASA/IPAC Extragalactic Database (NED) is operated by the Jet Propulsion Laboratory, California Institute of Technology, under contract with the National Aeronautics and Space Administration.

23 The reported uncertainty only accounts for statistical errors. The authors speculate that the systematic uncertainty could be of order 0.05 mag in distance modulus.
Overall, the agreement between our measurement and the results above is satisfactory given the uncertainties of the individual methods. However, the 15% deviation to the tailored EPM distance of Dessart et al. (2008) warrants investigation. We find that roughly half of the discrepancy arises from differences in the time of explosion. From the evolution of the ratio of photospheric angular diameter and velocity, Dessart et al. (2008) obtain an explosion epoch that is earlier than ours by about a day. These latter authors explain the difference between their estimate and those based on nondetections (specifically, Pastorello et al. 2006, in their paper) with a short time delay between the beginning of the expansion and the optical brightening. After adjusting the time of explosion, the remaining deviation is around 7% and thus within the expected range.

8. Conclusions and outlook

In this paper, we demonstrate the use of spectral emulation to predict the SN II spectra and magnitudes generated by Tardis (Kerzendorf & Sim 2014; Vogl et al. 2019). The key ingredient of our approach is the creation of a low-dimensional space for the interpolation of synthetic spectra through the combination of appropriate data preprocessing and dimensionality reduction by PCA. In this space, we train Gaussian processes to predict preprocessed, dimensionality-reduced spectra for new sets of input parameters. In the final step, we reverse the preprocessing procedure to obtain a spectrum that can be compared to observations. This method emulates the output of our radiative transfer code to high precision; we demonstrate this by comparing emulated and simulated spectra for a large number of test models. On average, the emulator prediction deviates from the simulation by around 0.64% (as measured by the MFE) – this is much smaller than both observational and model uncertainties. Not only are the interpolation uncertainties small but we can also estimate them sensibly through our use of Gaussian processes; this will allow us in the future to propagate these errors into the uncertainties of the inferred parameters.

We complement the spectral emulator with an emulator for absolute magnitudes; we have discarded the luminosity information in the spectral emulator to standardize the spectra and to obtain better predictive performance. The training data are Johnson-Cousins B, V, I magnitudes that have been synthesized from the unprocessed training spectra. We remove variations in the luminosity that result from differences in the physical sizes of the supernova models by transforming the magnitudes to the position of the photosphere; we then interpolate the transformed magnitudes using Gaussian processes. This allows us to predict absolute magnitudes with an average precision of better than 0.01 mag, which is significantly smaller than typical observational uncertainties.

The emulator is not only accurate but is also orders of magnitude faster (=10 ms) than our simulator TARDIS (=100,000 s) making it possible to fit spectra automatically. We demonstrate this by performing maximum likelihood parameter estimation for spectral time series of SN 1999em and SN 2005cs. The inferred parameters of the supernovae show good agreement with those of Dessart & Hillier (2006) and Dessart et al. (2008), who studied these objects using the CMFGEN code. Similarly, the distances that we infer from our fits are consistent with the best available measurements from the literature.

As a next step, we will develop a more detailed likelihood to infer accurate uncertainties for complete parameter estimates. The emulator and an advanced likelihood will then allow the use of type IIP supernovae for accurate cosmological distance determinations.

Acknowledgements. CV thanks AndreasFloers, MarcWilliamson, and MarkusKromer for stimulating discussions during various stages of this project. The authors gratefully acknowledge Stefan Taubenberger for sharing his enormous expertise in the field of supernovae and for being a key member of the supernova cosmology project that motivated this work. The authors thank the anonymous reviewer for valuable comments. This work has been supported by the Transregional Collaborative Research Center TRR3 “The Dark Universe” of the Deutsche Forschungsgemeinschaft and by the Cluster of Excellence “Origin and Structure of the Universe” at Munich Technical University. SAS acknowledges support from STFC through grant ST/P000312/1. This research made use of TARDIS, a community-developed software package for spectral synthesis in supernovae (Kerzendorf & Sim 2014; Kerzendorf et al. 2019). The development of TARDIS received support from the Google Summer of Code initiative and from ESA’s Summer of Code in Space program. TARDIS makes extensive use of Astropy and PyNE. Data analysis and visualization was performed using Matplotlib (Hunter 2007), NumPy (Oliphant 2006) and SciPy (Jones et al. 2001).
Appendix A: Min-max normalization

Min-max normalization scales each feature (here, the fluxes in a bin) individually such that it spans the range [Min, Max] for the training data. The min-max normalized flux $f_{\text{norm}}^{\lambda,i,j}$ for spectrum $i$ in bin $j$ is given by

$$f_{\text{norm}}^{\lambda,i,j} = \frac{f^{\lambda,i,j} - \min f^{\lambda,i,j}}{\max f^{\lambda,i,j} - \min f^{\lambda,i,j}} \times (\text{Max} - \text{Min}) + \text{Min}. \quad (A.1)$$

This linear transformation can be easily reversed in the prediction step of the emulator.