Modeling the disequilibrium species for Jupiter and Saturn: Implications for Juno and Saturn entry probe

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Abstract
Disequilibrium species have been used previously to probe the deep water abundances and the eddy diffusion coefficient for giant planets. In this paper, we present a diffusion-kinetics code that predicts the abundances of disequilibrium species in the tropospheres of Jupiter and Saturn with updated thermodynamic and kinetic data. The dependence on the deep water abundance and the eddy diffusion coefficient is investigated. We quantified the disagreements in CO kinetics that comes from using different reaction networks and identified C$_2$H$_6$ as a useful tracer for the eddy diffusion coefficient. We first apply a H/P/O reaction network to Jupiter and Saturn’s atmospheres and suggest a new PH$_3$ destruction pathway. New chemical pathways for SiH$_4$ and GeH$_4$ destruction are also suggested, and another AsH$_3$ destruction pathway is investigated thanks to new thermodynamic and kinetic data. These new models should enhance the interpretation of the measurement of disequilibrium species by JIRAM on board Juno and allow disentangling between methods for constraining the Saturn’s deep water abundance with the Saturn entry probes envisaged by NASA or ESA.

Keywords: Abundances, atmospheres – Jupiter, atmosphere – Saturn, atmosphere

1. Introduction
Disequilibrium species in the atmosphere of Jupiter and Saturn can be used to constrain the deep water abundance and the deep eddy diffusion coefficient in the atmospheres of Jupiter and Saturn (e.g., Prinn and Barshay 1977, Fegley and Lodders 1994). Various disequilibrium species such as CO, PH$_3$, GeH$_4$, and AsH$_3$ have been detected on Jupiter and Saturn with abundances orders of magnitude higher than their respective chemical equilibrium abundances at the pressure level where they are observable (e.g., Beer 1975, Noll et al. 1986, Ridgway et al. 1976, Larson et al. 1980, Fink et al. 1978, Noll et al. 1988, Bézard et al. 1989, Noll et al. 1989). These species at a few bars are transported upward by vertical mixing from the deep atmosphere where they are more abundant, therefore, they contain the information of the atmosphere down to a few hundred bars. In this paper, we model the vertical profiles of disequilibrium species with updated thermodynamic and kinetic data. The dependence on the water abundance and the eddy diffusion coefficient is investigated.

Our study is timely for the following reasons. The JIRAM instrument on board the Juno spacecraft will be able to measure the disequilibrium species CO, PH$_3$, GeH$_4$, and AsH$_3$ down to a few bars when it will arrive at Jupiter in 2016 (Grassi et al. 2010). The microwave radiometer onboard Juno will also be able to measure the deep water...
abundance (Janssen et al., 2005). With the abundances of disequilibrium species and water, constraints should be made on the deep eddy diffusion coefficient. A Saturn probe proposal has been submitted to the ESA 2015 call for medium class mission (Mousis et al., 2015) and a similar concept is under study for a submission to the NASA 2016 New Frontier call (Atkinson et al., 2012). Current entry probes are designed to go down to 10–20 bar and can make in-situ measurements of the atmosphere composition via mass spectrometry (Wong et al., 2004). However, it is unlikely that such probes will be able to descend below the water cloud deck and measure the deep water abundance. A study with the updated kinetic data is then necessary for evaluating whether deep water abundance can be effectively constrained by disequilibrium species.

We use the diffusion-kinetic model developed in Wang et al. (2015). A C/N/O/H reaction network is employed to predict the abundances of various carbon bearing species. The reaction networks for P/H/O and Si/H/O species are applied for the first time to study planetary atmospheres in this paper. New chemical pathways for PH$_3$ and GeH$_4$ destructions are then proposed. New compilations of thermochemical data, especially for P, Ge, and As, are used in our model.

The paper is organized as follows. In section 2, we introduce the current status of the measurement of disequilibrium species. In section 3, we describe our models for the chemistry and transport of disequilibrium species. In section 4, we present our results. In section 5, we discuss the implications for Juno and a Saturn entry probe. The conclusions are summarized in section 6.

2. Measurements of disequilibrium species: current status

The tropospheric abundances of CO, PH$_3$, SiH$_4$, GeH$_4$ and AsH$_3$ are primarily measured in the 5 µm window for Jupiter and Saturn. Apart from a 1 ppb tropospheric component (e.g., Larson et al., 1978; Bjoraker et al., 1986), CO also has a stratospheric component (e.g., Bézard et al., 2002). The tropospheric CO is supplied by vertical convective mixing from deep levels where CO prevails (Prinn and Barshay, 1977), while the stratospheric CO can be supplied by micrometeoroids (Prather et al., 1978), infalling materials from icy satellites (Strobel, 1979), or shock chemistry from infalling kilometer to subkilometer-sized comets (Lellouch et al., 1995; Bézard et al., 2002). At Jupiter and Saturn, comets are more probable than other sources (Bézard et al., 2002; Cavalié et al., 2010). The tropospheric CO contains information on the deep atmosphere, and thus can be used to probe the deep water abundance and the deep eddy diffusion coefficient. The retrieval of Saturn’s tropospheric CO has not been successful due to its very low mixing ratios (Cavalié et al., 2009). Tropospheric PH$_3$ was measured in the 5 µm window for Jupiter with a mixing ratio of $(6 - 9) \times 10^{-7}$ (e.g., Kunde et al., 1982; Bjoraker et al., 1986; Encrenaz et al., 1996; Irwin et al., 1998), and for Saturn with a mixing ratio of $(3 - 5) \times 10^{-6}$ (e.g., Noll and Larson, 1991) de Graauw et al. (1997) Fletcher et al. (2011). The vertical profile of PH$_3$ was retrieved from the spectra by Cassini CIRS and VIMS (Fletcher et al., 2009a, 2011). The PH$_3$ abundance starts to be depleted in the upper troposphere where the pressure is about 1 bar (Fletcher et al., 2012), due to decreased eddy mixing, UV photolysis and chemical re-equilibration (Irwin et al., 1998; 2004). Tropospheric GeH$_4$ was identified and measured at the 5 µm window (Fink et al., 1978; Noll et al., 1988) at a mixing ratio of a few times $10^{-10}$. The mixing ratio of GeH$_4$ in the stratosphere is expected to be lower than that in the troposphere because of UV photolysis. The tropospheric AsH$_3$ was measured on both Jupiter and Saturn (Bézard et al., 1989; Noll et al., 1989; Noll and Larson, 1991). The mixing ratio of AsH$_3$ on Jupiter is about $2 \times 10^{-10}$ (Noll et al., 1990), while for the Saturn, the mixing ratio is about $3 \times 10^{-7}$ (Bézard et al., 1989; Noll and Larson, 1991). In table 1, we summarize the measurements of tropospheric CO, PH$_3$, SiH$_4$, GeH$_4$, and AsH$_3$ abundances for both Jupiter and Saturn.

3. Model

3.1. Introduction to the model

We developed a code to solve the 1-D transport-kinetic equation:

$$\frac{\partial Y_i}{\partial t} = \frac{1}{\rho} \frac{\partial}{\partial z} \left( \rho K_{\text{eddy}} \frac{\partial Y_i}{\partial z} \right) + P_i - L_i,$$

where $Y_i$ is the mass fraction of species i, $\rho$ is the density of the atmosphere, $z$ is the vertical coordinate relative to a reference point in the atmosphere (we choose the 1 bar level in the code), $K_{\text{eddy}}$ is the vertical eddy diffusion coefficient,
\( P_i \) is the chemical production rate of species \( i \), and \( L_i \) is the chemical loss rate of species \( i \). Both \( P_i \) and \( L_i \) have a unit of \( \text{g cm}^{-3} \text{s}^{-1} \). The time evolution of \( Y_i \) is controlled by two physical processes: one is the chemical production and destruction of species \( i \), and the other is its corresponding vertical transport. In the convective envelope of Jupiter and Saturn, the transport of mass is mainly by turbulent convection. Here in equation (1), the convective transport of species is approximated by diffusion transport with an coefficient \( K_{\text{eddy}} \), which is a good approximation justified by the success of mixing length theory in explaining stellar convection (Stone, 1976). The mass fractions \( Y_i \) are initialized using their local chemical equilibrium values along the adiabat. The chemical net production rate \( (P_i - L_i) \) is integrated using Cantera, a software toolkit developed for problems involving chemical kinetics and thermodynamics (Goodwin et al., 2015). At each time step, we call Cantera to do the integration and include the result in the resolution of the continuity equation. Cantera has been used and tested for many applications including combustion, detonation, fuel cells, batteries, etc. The integration is terminated when the mass fractions \( Y_i \) reach steady state. The code requires three kinds of input. One is the temperature pressure profile \((T - P)\) profile, the second is a list of thermodynamic properties in the format of NASA polynomials (McBride et al., 1993) for each species, and a list of reactions between these species, the third is the elemental composition and the vertical eddy diffusion coefficient \( K_{\text{eddy}} \).

The \((T - P)\) profiles for Jupiter and Saturn are calculated following the method described in Fegley and Prinn (1985). We choose a reference point where temperature and pressure are measured and extrapolated into the deep atmosphere assuming a dry adiabat. For Jupiter, we use \( T = 427.71 \text{ K} \) at 22 bars as our reference point (Seiff et al., 1998). The pressure and temperature conditions lower than 22 bars are from the Galileo entry probe measurements (Seiff et al., 1998). For Saturn, we use \( T = 134.8 \text{ K} \) at \( P = 1 \text{ bar} \) as our reference point (Lindal et al., 1985). The heat capacity of the atmosphere used in the calculation is computed by linearly combining the heat capacities of \( H_2 \) and \( He \), and the heat capacities of \( H_2 \) and \( He \) are from NIST-JANAF thermochemical table (Chase, 1998). The helium mixing ratio we use is 0.157 for Jupiter (Niemann et al., 1998) and 0.135 for Saturn (Conrath and Gautier, 2000). The \((T - P)\) profiles for Jupiter and Saturn are calculated and shown in Fig. 1. The thermodynamic and reaction data are gathered from various sources which are detailed in the following:

- **C/N/O/H reaction network**

  Our C/N/O/H reaction network used in this paper is developed based on the network from Venot et al. (2012) downloaded from the KIDA database (Wakelam et al., 2012, http://kida.obs.u-bordeaux1.fr). The network consists of 105 neutral species and 963 reactions. Among the reactions, 957 of them are reversible reactions and 6 of them are irreversible reactions. A complete list of the species can be found in Venot et al. (2012). The network has been validated against various combustion experiments in the temperature range between 300 K and 2000 K and in the pressure range between 0.01 bar and several hundred bars.

  Alternative network applied to the hydrogen-rich atmospheres is that of Moses et al. (2011) and Visscher and Moses (2011). Moses (2014) compared their model with the Venot et al. (2012) model and found that the major difference in CO/CH\(_4\) chemistry comes from the rate coefficient of the reaction \( H + CH_3OH \leftrightarrow CH_3 + H_2O \). The Venot et al. (2012) model used the rate coefficient obtained by Hidaka et al. (1989) from laboratory experiments. However, Moses (2014) argued that this reaction likely is prohibited by a very large energy barrier and is much slower than was estimated by Hidaka et al. (1989) based on quantum chemical calculations in Moses et al. (2011). It remains to be seen whether changing the rate coefficient following the suggestions by Moses et al. (2011) would reproduce the experimental results in Hidaka et al. (1989). Therefore, because the discrepancy remains unresolved, we have considered two reaction networks in our model, which are:

  - **network A**: it is based on the Venot et al. (2012) network with some modifications. Among the species in the list, we remove HNC because it does not participate in any reactions in the reaction network. We include CH\(_3\)HN\(_2\), CH\(_3\)HN, CH\(_2\)NH\(_2\), and CH\(_2\)NH into the network since these species are expected to be important in a hydrogen rich environment (Moses et al., 2010). The final network A consists of 108 species and 1000 reactions. Added reactions and their rate coefficients are from Dean and Bozzelli (2000). The thermodynamic properties are mainly compiled from Burcat and Rusceci (2005), McBride et al. (1993), Dean and Bozzelli (2000), and Venot et al. (2012). An online updated version of the Burcat and Rusceci (2005) database can be found at http://garfield.chem.elte.hu/Burcat/burcat.html. The whole reaction list along with thermodynamic data and rate coefficient data are available in the KIDA database (http://kida.obs.u-bordeaux1.fr/networks.html).
We use the quenching timescale approach to compute the abundances of GeH utilized thermodynamic properties. Indeed, we have changed the thermodynamic data to those provided in Venot 2. Evolution is very similar for H and OH, but not exactly the same for C and NNH. A comparison between our results and those from the nominal model of Venot et al. (2012) is shown in Fig. 2. The calculation using the NASA Chemical Equilibrium Application (CEA) (Gordon and McBride, 1994; McBride and Gordon, 1996) for temperature and pressure conditions along the adiabats of Jupiter and Saturn is important but missing from this reaction network, so we added it and associated reactions into the reaction network. The thermodynamic data are primarily from Burcat and Ruscic (2005), McBride et al. (1993). The SiO/O reaction network is based on Twarowski (1995). The reaction network consists of 24 species and 175 reactions. The phosphorus containing species included are: PH, PH2, PHOPO, HPO, PO, PO2, PO3, HOPO2, P2O5, P, P2, P4, P2O, P2O5, HPOH, H2POH. The network has been used to explain the faster recombination rate of H and OH in the presence of phosphine combustion products (Twarowski, 1996). To make sure all important species under Jupiter/Saturn’s atmospheric conditions are included, we performed an equilibrium calculation using the NASA Chemical Equilibrium Application (CEA) (Gordon and McBride, 1994; McBride and Gordon, 1996) for temperature and pressure conditions along the adiabats of Jupiter and Saturn. We find H2PO4 is important but missing from this reaction network, so we added it and associated reactions into the reaction network. The thermodynamic data for P2O and PO2 are from Twarowski (1993). The whole reaction network is available in the KIDA database.

For arsenic (As) and germanium (Ge) containing species, there is no reaction network available in the literature. We use the quenching timescale approach to compute the abundances of GeH and AsH3 along Jovian and Saturnian adiabats. This approach does not need a whole reaction network but a single rate determining step. This method was widely used in the literature as an alternative to the diffusion-kinetic modeling (e.g., Prinn and Barshay, 1977; Fegley and Lodders, 1994), and can correctly predict the quench level as long as the appropriate rate determining step is used and the recipe in Smith (1998) is followed to compute the mixing timescale. A detailed description of this approach can be found in Wang et al. (2015).

For equilibrium computations, we use the NASA Chemical Equilibrium Application (CEA) as our reference (Gordon and McBride, 1994; McBride and Gordon, 1996). This code is in wide use in the aerodynamic and thermodynamic community. The code includes over 2000 species in the database.

The elemental abundances of Jupiter and Saturn used in this paper are summarized in Table 2. We use the solar composition table from Asplund et al. (2009) as our reference. The elemental abundances are inferred from the observed abundances of their hydrogen compounds. For phosphorus, we assume the total phosphorus abundance is equal to the observed PH3 abundance. For silicon and germanium, we assume they have enrichments similar to carbon, since their observed hydrogen compounds (SiH4 and GeH4) do not represent their total elemental abundances. For arsenic, we assume its total abundance is represented by the observed AsH3 abundance.

3.2. Validation of the Diffusion-Kinetic Code

We first test our code without diffusion using the C/N/O/H reaction network computing the time evolution of the abundances of different species at constant temperature and pressure. The integration is done using Cantera. A comparison between our results and those from the nominal model of Venot et al. (2012) is shown in Fig. 2. The evolution is very similar for H and OH, but not exactly the same for C2H6 and NNH. The difference is due to the utilized thermodynamic properties. Indeed, we have changed the thermodynamic data to those provided in Venot et al. (2012) and exactly obtained the same evolution of the abundance profiles for all four species. This prompts us
to compare the thermodynamic data we used with those in Venot et al. (2012). Our thermodynamic data are gathered from widely used compilations, for example, McBride et al. (1993) and Burcat and Rusch (2005). The species that are not available from literature are estimated using the software THERM (Ritter, 1991). Venot et al. (2012) also gathered thermodynamic data in a similar manner. However, we do not know the source of thermodynamic data for each species in Venot et al. (2012), therefore, comparisons for individual species is not possible. This is not expected to be a major source of uncertainty since the uncertainties in the kinetic data are much larger than those in the thermodynamic data.

The test with both kinetics and diffusion is done by simulating the Saturn’s atmosphere thermochemistry using the C/N/O/H reaction network, and comparing against the results in Fig. 1 of Mousis et al. (2014). The reference result in Mousis et al. (2014) for Saturn is computed using the same code as in Venot et al. (2012). The comparison, represented in Fig. 3 shows that the differences in the mixing ratios are within 10%. There might be three sources of error that contribute to the differences of the mixing ratios shown in Fig. 3; (1) the temperature-pressure profile; (2) the thermodynamic data; (3) the elemental abundances, which are all inputs to our code. These difference are small and the comparison shows our code can correctly solve the diffusion-kinetics Equation (1).

4. Results

In this section, we predict the abundances of various disequilibrium species in Jupiter’s and Saturn’s atmospheres at a few bars pressure. Above this level altitude, the abundances are affected by photochemistry and the enrichment from external sources, which are not included in our calculations here. The dependence on the water abundance and the deep eddy diffusion coefficient are investigated.

We make a few definitions regarding the abundance of species Z. Its concentration is denoted as [Z] with units of molecules·cm$^{-3}$. Mole fraction of Z is denoted as $X_Z = [Z]/n$, where $n$ is total number density of the atmosphere (molecule·cm$^{-3}$). Mixing ratio is denoted as $q_Z = [Z]/[H_2]$. For an element M, we define $E_M$ as the enrichment of M relative to solar, which is the ratio of [M]/[H] in the planet to that in the Sun, where [M] and [H] are the total number density of M and H atoms respectively, in whatever form. The elemental composition of the solar atmosphere is taken from Asplund et al. (2009). The elemental abundances of Jupiter and Saturn used in our simulations can be found in Table 2.
The tropospheric CO abundance on Jupiter was measured at the Northern Equatorial Belt (∼ 9°) by Bézard et al. (2002) with a mole fraction of (1.0 ± 0.2) × 10⁻⁹. Combined with the predicted eddy diffusion coefficient of ∼ 1 × 10⁸ cm²s⁻¹ (Wang et al., 2015) near the equatorial regions, the deep water abundance is constrained to be ∼ 7 times solar with network A and ∼ 0.6 times solar with network B.

The simulation results for Saturn are presented in Fig. 5. Similarly to the results for Jupiter, we find CH₃ is a good tracer for the eddy diffusion coefficient. Both CO and CO₂ are good tracers for the deep water abundance. Dual constraints from CO and CH₃ can break the degeneracy between high (low) eddy diffusion coefficient and high (low) deep water abundance.

The tropospheric CO abundance on Saturn was not measured so far and an upper limit is put by Cavalié et al. (2009) with a mixing ratio smaller than 1 ppb. Combined with the predicted eddy diffusion coefficient of ∼ 1 × 10⁸ cm²s⁻¹ (Wang et al., 2015) near the equator, the deep water abundance is constrained to be ≤ 60 times solar with network A and ≤ 10 times solar with network B.

4.2. Simulation results using the H/P/O reaction network

We use the NASA CEA chemical equilibrium code to compute the equilibrium abundances of phosphorus containing species along Saturn’s adiabat, and the results are shown in Fig. 6. The elemental abundances used in the calculations are summarized in Table 2. Our calculations show that H₃PO₄ is the major phosphorus bearing species below 700 K instead of P₄O₆ in the literature (e.g., Fegley and Lodders, 1994; Visscher and Fegley, 2005). We find the difference is due to the different thermodynamic data used for P₄O₆. Fegley and Lodders (1994) and others use the standard enthalpy of formation of P₄O₆ (ΔH°[P₄O₆]) from JANAF table (Chase et al., 1985), which is based on the experiments by Koerner and Daniels (1952). As a comparison, the CEA code uses the ΔH°[P₄O₆] from Gurvich’s table (Gurvich and Veyts, 1990), which is based on the experiments by Hartley and McCoubrey (1963). Fegley and Lodders (1994) favored the data from the JANAF table because they see “no compelling reasons, such as a problem with experimental methods or data reduction, to reject the work of Koerner and Daniels (1952) in favor of the work of Hartley and McCoubrey (1963).” They point out that the discrepancy needs to be resolved by a new experimental determination of the ΔH°[P₄O₆]. However, we favor the data from Gurvich’s table for the following reasons. Hartley and McCoubrey (1963) actually pointed out that in the experiment of Koerner and Daniels (1952) the sample examined is a mixture of P₄O₆ and P₄O₁₀ rather than pure P₄O₆. The identification of P₄O₆ is not necessarily definitive and it may lead to the more negative values of the enthalpy of formation for P₄O₆ (due to pollution by P₄O₁₀). Later studies by Muenow et al. (1970) and Smoes and Drowart (1973) also supported the measurement by Hartley and McCoubrey (1963). Quantum chemical calculations by Morgan (2012) get values of the enthalpy of formation of P₄O₆ that are closer to the values of Hartley and McCoubrey (1963). We didn’t find another direct or indirect measurement that supported the values by Koerner and Daniels (1952). The Burcat database (Burcat and Ruscic, 2005) adopted the values by Hartley and McCoubrey (1963) and pointed out that the values used in JANAF is erroneous. For these reasons, we choose to take the data from Gurvich’s table. Our computation shows that PH₃ is converted to H₃PO₄ at about 700 K in Saturn’s atmosphere. From our computations for Jupiter, PH₃ is largely converted to H₃PO₄ at about 650 K in Jupiter’s atmosphere.

The main chemical pathway for PH₃/H₃PO₄ conversion is identified from the H/P/O reaction network by comparing the rates of all the reactions in the network. This method is very robust since no information is needed other than the kinetic data. The details of our analysis are presented in the Appendix B. We find the main chemical pathway consists of the following reactions:
The rate determining step for the pathway is reaction (2h). The rate coefficient for this reaction is estimated in [Twarowski 1995]. For the reverse reaction of (2h), the rate coefficient \( k_{eq} = 5.24 \times 10^{-11} e^{-6014/T} \text{ cm}^3 \text{ molecule}^{-1} \text{s}^{-1} \). Using the detailed balance, the forward rate coefficient \( k_2 = k_{eq} K_{eq} \), where \( K_{eq} \) is the equilibrium constant of reaction (2h). Therefore, the forward rate coefficient is estimated to be \( k_2 = 2.35 \times 10^{-12} e^{-1.067 \times 10^4/T} \text{ cm}^3 \text{ molecule}^{-1} \text{s}^{-1} \).

In Figures 7 and 8, we have plotted the predicted mixing ratios of PH as a function of the \( K_{eddy} \) computed using the rate determining step. Our calculations show that the mixing ratio of PH is not sensitive to the values of \( K_{eddy} \) unless \( K_{eddy} \) is less than \( 1 \times 10^5 \) cm\(^3\) s\(^{-1}\). We also compared the predicted PH for different values of \( E_{H_2O} \). The mixing ratio of PH is also not sensitive to the value of \( E_{H_2O} \) unless \( E_{H_2O} \) is greater than 30. PH’s insensitivity to parameters is due to its quench level deep in the regime where it is the dominant species. For example, when \( K_{eddy} = 1 \times 10^7 \) cm\(^3\) s\(^{-1}\) and \( E_{H_2O} = 10 \), the quench level is at \( T \approx 900 \text{K} \). From our equilibrium calculations shown in Fig. 6, PH is stable and dominant until below 700 K. Almost all the phosphorus is sequestered in PH on Jupiter and Saturn.

**4.3. Simulation results for SiH\(_4\)**

Figure 9 shows the predicted equilibrium abundances of some Si-bearing species along Saturn’s adiabat computed using the NASA CEA code. The elemental abundances used in the calculations are summarized in Table 2. MgSiO\(_3\) (1s) and Mg\(_2\)SiO\(_4\) (s) condensate are the primary carriers of Si below 2000 K. The mixing ratio of SiH\(_4\) is \( 1 \times 10^{-9} \) at about 1500 K, and decreases to \( 1 \times 10^{-18} \) at about 1000 K. The equilibrium results are in agreement with the results from Fegley and Lodders [1994]. Observationally, the upper limit for \( q_{SiH_4} \) on Jupiter is \( 2.5 \times 10^{-9} \) [Treffers et al., 1978], and the upper limit for \( q_{SiH_4} \) on Saturn is \( 2.0 \times 10^{-10} \) [Noll and Larson, 1991]. This indicates that almost all of the silicon on Jupiter and Saturn is removed by the rock formation and subsequent condensation. The total oxygen in Jupiter should be at least the oxygen locked in the rocks (e.g., Visscher and Fegley, 2005). Since MgSiO\(_3\) (s) is the major condensates for silicon, each silicon atom is combined with three oxygen atoms. Assuming the total silicon enrichment relative to solar is similar to the enrichment for carbon, then Si/H is about \( 1.43 \times 10^{-4} \) on Jupiter and \( 3.24 \times 10^{-4} \) on Saturn. The oxygen locked with silicon therefore has a mixing ratio of \( O/H > 4.4 \times 10^{-4} \) for Jupiter and \( O/H > 1.0 \times 10^{-3} \) for Jupiter and Saturn, corresponding to about 0.9 and 2.0 times solar, respectively. Adding this part of oxygen and the oxygen sequestered in water would give the total oxygen in Jupiter and Saturn.

Thanks to the detailed kinetic data of Miller et al. [2004], we can extract the main chemical pathway for SiH\(_4\) destruction from the reaction network. The main chemical pathway is identified by comparing the rates of all the reactions in the network. The analysis is detailed in the Appendix C. The main chemical pathway of SiH\(_4\) destruction is given by the following reactions:

\[
\begin{align*}
PH_3 & \leftrightarrow PH_2 + H \quad (2a) \\
PH_2 + H_2O & \leftrightarrow H_2POH + H \quad (2b) \\
H_2POH + PH_2 & \leftrightarrow HPOH + PH_3 \quad (2c) \\
HPOH & \leftrightarrow HPO + H \quad (2d) \\
HPO & \leftrightarrow PO + H \quad (2e) \\
PO + H_2O & \leftrightarrow HOPO + H \quad (2f) \\
HOPO + H & \leftrightarrow PO_2 + H_2 \quad (2g) \\
PO_2 + H_2O & \leftrightarrow HOPO_2 + H \quad (2h) \\
HOPO_2 + H_2O & \leftrightarrow H_3PO_4 \quad (2i) \\
\end{align*}
\]

\[\text{PH}_3 + 4 \text{H}_2\text{O} \leftrightarrow \text{H}_3\text{PO}_4 + 4\text{H}_2 \quad (\text{2 network})\]
SiH₄ + M ↔ SiH₂ + H₂ + M.  
SiH₂ + H₂O ↔ HOSiH + H₂,  
HSiOH ↔ SiO + H₂,  
SiO + H₂O ↔ Si(OH)₂,  
Si(OH)₂ + H ↔ HOSiO + H₂,  
Si(OH)₂ ↔ HSO(OH)  
HSiO(OH) + H ↔ HOSiO + H₂,  
HOSiO ↔ SiO₂(cr) + H,  
SiO₂(cr) + Mg(OH)₂ ↔ MgSiO₃(s) + H₂O.  

The steps (3a) to (3i) are directly identified from the network, but the last step (3i) is added because SiO₂(cr) is not a stable product in the atmospheres of Jupiter and Saturn according our equilibrium calculations and those of [Fegley and Lodders, 1994]. A reaction incorporating Si into to MgSiO₃(s) completes the chemical pathway. Compared with the chemical path proposed in Fegley and Lodders (1994), the formation of SiH₂ and MgSiO₃(s) is the same, but the path from SiH₂ to SiO₂(cr) is different. The difference is due to the methodologies used to identify main chemical pathways. Fegley and Lodders (1994) constructed their chemical pathway by identifying important intermediates observed in the experiments and then devising a pathway to connect the reactants, intermediates, and the products. There might be other important intermediates that are missing from the pathway, and the way of connection is not unique. This method is used when we do not have a reaction network or do not have enough kinetic data to perform detailed analysis. However, since we now have a reaction network, we can simulate the chemical evolution using the network and identify the fastest route from SiH₂ to SiO₂(cr). Our analysis is detailed in the Appendix C. Among the chemical pathway, we find reactions [3a], [3b], and [3g] all serve as the bottlenecks. There is no unique rate limiting step for SiH₂ destruction.

This analysis helps us simplify the original H/Si/O reaction network from Miller et al. (2004). The original network is designed for the simulation of SiH₂ burning in the molecular oxygen. Therefore, the composition is silicon-rich and oxygen-rich. However, the atmosphere of Jupiter and Saturn is hydrogen rich. Some species in the reaction network are expected to be unimportant in Jupiter and Saturn’s atmosphere, and thus can be removed from the network to increase the efficiency of time integration. In the simplified reaction network, the species included are H₂, He, H₂O, OH, H, SiH₂, SiH₄, SiO, Si(OH)₂, HSiOH, HSiO(OH), HOSiO, and SiO₂(c). These species are the major intermediates for SiH₂ destruction, as is shown in Fig. C.20 in the Appendix C. This simplified reaction network is used to predict the abundance of SiH₂ along Saturn’s adiabat for different values of K_{edd} and E₀. The results are presented in Fig. 10. For E₀ = 2 and K_{edd} = 1×10³ cm² s⁻¹, the predicted mixing ratio of SiH₂ at a few bars level is about 1×10⁻¹⁸, while for E₀ = 30 and K_{edd} = 1×10⁴ cm² s⁻¹, the mixing ratio of SiH₂ falls to 1×10⁻²⁸. For the two extreme cases considered here, SiH₂ abundance is too small to be detected. Therefore, we conclude SiH₂ is not expected in Saturn’s troposphere. The same analysis is applied to Jupiter. Similar to the result for Saturn, SiH₂ is also not expected in Jupiter’s troposphere. Fegley and Lodders (1994)’s calculation for SiH₂ kinetics also concludes the low mixing ratio of SiH₂. We confirm this result using a new Si/H/O reaction network.

4.4. Simulation results for GeH₄

In Fig. 11 we show the equilibrium abundances of germanium containing species along Saturn’s adiabat computed using the NASA CEA code. The elemental abundances used in the calculations are summarized in Table 2. The figures show that GeH₄ is not the dominating germanium containing species, and it is converted to more abundant GeS at lower temperature. Condensation happens near 700 K, and the major condensates are Ge(cr), GeSi(cr) and GeO₂(cr). There are limited data for the GeH₄ kinetics, therefore, we propose a chemical pathway for the conversion between GeH₄ and GeS by analogy with SiH₂ and SiO, since Si and Ge are in the same group and next to each other in the periodic table, and O and S are in the same group and also next to each other in the periodic table. The main chemical
pathway for the conversion from SiH to SiO is given by reactions 3a, 3b, and 3c. The rate determining reaction is 3b. By analogy, we propose the main chemical pathway below for the conversion from GeH₄ to GeS.

\[
\text{GeH}_4 + M \leftrightarrow \text{GeH}_2 + H_2 + M, \quad (4a)
\]
\[
\text{GeH}_2 + H_2S \leftrightarrow \text{HSGeH} + H_2, \quad (4b)
\]
\[
\text{HSGeH} \leftrightarrow \text{GeS} + H_2, \quad (4c)
\]

and the rate determining reaction is 4b. This chemical pathway is very similar to the one proposed in Fegley and Lodders (1994). The only difference is the step from GeH₂ to HSGeH. In Fegley and Lodders (1994), two steps are used: the first is GeH₂ + H₂S ↔ H₂Ge=S + H₂, and the second is H₂Ge=S ↔ HGe=SH. In the H/Si/O reaction network, the rate coefficient for SiH₂ + H₂O ↔ H₂Si=O + H₂ is 3.84 × 10^{10} T^{-0.6} e^{−4958/T} \text{ cm}^3 \text{ mol}^{-1} \text{s}^{-1}, and the rate coefficient for SiH₂ + H₂O ↔ HSi=OH + H₂ is 2.15 × 10^{10} T^{0.7} e^{−4958/T} \text{ cm}^3 \text{ mol}^{-1} \text{s}^{-1} (Zachariah and Tsang 1995). At 800 K, the first reaction is much slower than the second reaction. By analogy, we therefore favor the single step from GeH₂ to HGe=SH proposed here instead of the double step proposed in Fegley and Lodders (1994).

The rate coefficient for the reaction 4b is not in the literature. Again by analogy with reaction SiH₂ + H₂O, we use \( K_e \approx 2.15 \times 10^{10} T^{0.7} e^{−4958/T} \text{ cm}^3 \text{ mol}^{-1} \text{s}^{-1} \) (Zachariah and Tsang 1995). The predicted mole fraction of GeH₄ as a function of the vertical eddy diffusion coefficient \( K_{\text{eddy}} \) is shown in Fig. 12 and 13 for Jupiter and Saturn, respectively. For Jupiter, our predicted mole fraction is consistent with the observed mixing ratio of \( 7.5 \times 10^{-10} \) by Bjorker et al. (1986) with the values of \( K_{\text{eddy}} \) predicted by Wang et al. (2015). For Saturn, our predicted mole fraction is also consistent with the observed value of \( (4±2)\times10^{-10} \) by Noll et al. (1998). This consistency indicates the rate coefficient of GeH₂ + H₂S is close to our estimate here. Within a factor 5 uncertainty on both sides of the rate coefficient (total factor of 25), we find the predicted mixing ratios of GeH₂ in agreement with the observed values. Adjusting the rate coefficient even higher or lower will yield a disagreement between the prediction and the observation. Therefore, the rate coefficient of reaction 4b should be within a factor of 5 of our estimation. When we have an accurate measurement of the rate coefficient, we can use the GeH₄ abundance to constrain the value of \( K_{\text{eddy}} \). The sensitivity of GeH₂ abundance on the \( K_{\text{eddy}} \) implies the effectiveness of using GeH₄ abundances to constrain the \( K_{\text{eddy}} \), but the kinetics needs to be better constrained by laboratory measurements first.

4.5. Simulation results for AsH₃

Equilibrium calculations show that AsH₃ is the dominant arsenic bearing species until it is converted to As₄ or As₂S₂ at about 400 K (Fegley and Lodders 1994). Due to the lack of kinetic data, it is quite uncertain where the quench level is. Fegley and Lodders (1994) proposed three possible chemical pathways of the conversion from AsH₃ to As₄ or As₂S₂. The first pathway starts from the combination of AsH and AsH₃ forming As₂H₂, then As₂H₂ is decomposed into As₂ which combines to form the As₄ condensates. A similar mechanism starts from two AsH₂ forming the As₂H₂, and the rest is the same. The third one start from the combination of AsH with HS forming AsS, and two AsS combines to form the As₂S₂ condensates. The first and the third chemical pathway were investigated by Fegley and Lodders (1994). The second one was not investigated because the authors do not have the thermodynamic data for AsH₂. However, the second pathway is more likely than the first pathway since AsH₂ is expected to be more abundant than AsH. Now we study the second pathway, which is described by the following reactions:

\[
\text{AsH}_3 + H \leftrightarrow \text{AsH}_2 + \text{H}_2, \quad (5a)
\]
\[
\text{AsH}_2 + \text{AsH}_2 \leftrightarrow \text{As}_2 \text{H}_2 + \text{H}_2, \quad (5b)
\]
\[
\text{As}_2 \text{H}_2 \leftrightarrow \text{As}_2 + \text{H}_2, \quad (5c)
\]
\[
\text{As}_2 + \text{As}_2 \leftrightarrow \text{As}_4, \quad (5d)
\]
\[
\text{As}_4 \leftrightarrow \text{As}_4(s), \quad (5e)
\]

where the rate determining step is taken as the reaction 5e. The thermodynamic data for AsH₃ is from Tirtowidjijo and Pollard (1986). The rate coefficient of the reaction 5e is taken as \( 4.63 \times 10^{-11} T^{0.04} e^{−16.8/T} \text{ cm}^3 \text{ molecule}^{-1} \text{s}^{-1} \), by analogy with the rate coefficient of SiH₂ + SiH₂ (Dollet and de Persis 2007). The analogy between As and Si is
probably not good, but we are forced by the lack of kinetic data for elements in the same column. We consider an overall two order of magnitude uncertainty for the rate coefficient. The kinetic results are shown in Fig. 14 and 15. From our calculations, the predicted AsH$_3$ abundance is nearly equal to the total arsenic abundance for a large range of the $K_{\text{eddy}}$. Now with the three chemical pathways studied, the conclusion is that AsH$_3$ abundance is not sensitive to the value of $K_{\text{eddy}}$, and AsH$_3$/H = As/H in both Jupiter and Saturn. The AsH$_3$ is observed on Jupiter with a mixing ratio of (2.2 ± 1.1) $\times$ 10$^{-10}$ (Noll et al. [1990], corresponding to 0.3–0.8 times solar abundance. The AsH$_3$ is observed on Saturn with a mixing ratio of (3 ± 1) $\times$ 10$^{-9}$ (Bézard et al. [1989], Noll et al. [1989], Noll and Larson [1991]), corresponding to 5–10 times solar abundance. The higher enrichment of As on Saturn than on Jupiter is consistent with other elements, such as C and P. However, the subsolar As/H ratio on Jupiter is puzzling because other rock forming elements such as phosphorus and germanium are all enriched relative to solar (e.g., Fegley and Lodders [1994]). There could be three possibilities. One is the observations have underestimated the AsH$_3$ abundance in Jupiter, and the AsH$_3$ abundance could be higher than solar. The second possibility is the observations are correct, but the kinetics are not. This may be hard to understand since the kinetics work well for Saturn. The third possibility is both observations and the kinetics are correct, and the subsolar abundance of As is realistic, but then a mechanism is needed to deplete arsenic on Jupiter. The JIRAM instrument on board Juno spacecraft has the capability of measuring the AsH$_3$ abundance at a few bars in Jupiter’s atmosphere (Grassi et al. 2010). However, to resolve this issue, experimental measurements on AsH$_3$ are necessary to better determine the arsenic kinetics.

5. Discussion

In section 4, we have presented our modeling results on the disequilibrium species using updated thermodynamic and kinetic data for Jupiter and Saturn. We have explored the dependence on the two free parameters in our model: the eddy diffusion coefficient and the deep water abundance. We find that CO and CO$_2$ are sensitive to both the eddy diffusion coefficient and the deep water abundance, while C$_2$H$_6$ and GeH$_4$ are only sensitive to the eddy diffusion coefficient. In this section, we discuss how Juno and a Saturn probe can improve our understanding on the $K_{\text{eddy}}$ and $E_{\text{H,CO}}$ through the measurement of disequilibrium species. We also discuss the uncertainties on the kinetic networks and suggest reactions that should be further studied.

5.1. Further constraints by Juno

Juno is about to arrive at Jupiter in July 2016, and the microwave radiometer is expected to map the water abundance down to ~100 bars. The JIRAM instrument will measure the abundances of H$_2$O, NH$_3$, PH$_3$, CO, GeH$_4$, AsH$_3$ at a few bars level (Grassi et al. 2010). Using the measured deep water abundance and the tropospheric CO abundance measured by Bézard et al. (2002), the eddy diffusion coefficient can be constrained as is shown by Fig. 4 in this paper and Fig. 5 in Wang et al. (2015). Another constraint on the $K_{\text{eddy}}$ can be placed using the measured GeH$_4$ abundance, as is shown by Fig. 12. However, a quantified reaction network is needed, or at least a determination of the rate limiting reaction is required to reduce the uncertainties in GeH$_4$ kinetics.

Both Flasar and Gierasch [1978] and Wang et al. (2015) predicted latitudinal variations on the deep eddy diffusion coefficient due to the rotational effects on the convection. The latitudinal variation of the eddy diffusion coefficient should result in latitudinal variations of the abundances of CO, C$_2$H$_6$, CO$_2$, and GeH$_4$ at a few bars level. Multi-latitude measurements of CO and GeH$_4$ will test the prediction, if performed by JIRAM. We predict no latitudinal variation on the PH$_3$ and AsH$_3$ abundances since their abundances are not sensitive to the eddy diffusion coefficient. The horizontal (latitudinal) profile of CO on Jupiter is presented in the Fig. 9 of Wang et al. (2015). The mole fraction of CO is predicted to be about 1 $\times$ 10$^{-9}$ near the equator and decreases to about 4 $\times$ 10$^{-9}$ near the pole. Fig. 10 of Wang et al. (2015) shows latitudinal variations of PH$_3$ on Jupiter because the old chemical model is used in that paper. With the new chemical model for phosphorus in this paper, we predict no latitudinal variations for PH$_3$ at a few bars level. The predicted horizontal profile of GeH$_4$ is shown in Fig. 16. The horizontal profile of eddy diffusion coefficient used in the calculations is from Wang et al. (2015). The mole fraction of GeH$_4$ is predicted to be about 7×10$^{-10}$ near the equator and slowly decreases to about 3×10$^{-10}$ near the pole.
5.2. Application to a Saturn entry probe

A Saturn entry probe with a mass spectrometer on board will be able to make in-situ measurements of the composition of Saturn, including the abundances of various disequilibrium species at a few bars level. The mass spectrometer is expected to have much higher resolution than the one on the Galileo entry probe. Therefore, it has the capability to make more precise and sensitive measurements. The probe may not be able to descend below the water cloud deck, and therefore cannot really determine the deep (global) water abundance. However, as is shown by Fig. 5, if both \( \text{C}_2\text{H}_6 \) and \( \text{CO} \) can be measured, useful constraints can be placed on both the eddy diffusion coefficient and the deep water abundance. The mixing ratio of \( \text{C}_2\text{H}_6 \) on Saturn is predicted to be about \( 1 \times 10^{-9} \), and the mixing ratio of the tropospheric \( \text{CO} \) is predicted to be below \( 1 \times 10^{-9} \). Therefore, any instrument must be sensitive enough to measure sub-ppb level of mixing ratios.

In addition, since \( \text{CO} \) and \( \text{N}_2 \) have nearly identical molecular weight, the payload must resolve the ppb level \( \text{CO} \) from the ppm level \( \text{N}_2 \). In [Wang et al., 2015], we predicted a higher eddy diffusion coefficient near the equator and a decreasing eddy diffusion coefficient at higher latitudes. Therefore, we expect \( \text{CO} \) and \( \text{C}_2\text{H}_6 \) to be higher in abundance near the equator. The probe entry site should be preferentially near the equator in order to maximize the possibility of detecting \( \text{CO} \) and \( \text{C}_2\text{H}_6 \). The mixing ratio of \( \text{GeH}_4 \) is predicted to be a few times \( 10^{-10} \), and is a sensitive function of the eddy diffusion coefficient. The measurement of \( \text{GeH}_4 \) can add another constraint on the eddy diffusion coefficient.

The Juno mission measurements provide a potentially important synergy with the Saturn Probe measurements. By measuring both the deep water abundance and disequilibrium species, it will be possible to determine both the deep oxygen abundance and the magnitude of vertical eddy mixing. The latter determination is especially robust if the disequilibrium species are measured as a function of latitude [Wang et al., 2015]. Having a determination of the Jovian value of the eddy mixing will provide a useful constraint on that for Saturn, which will help lift the degeneracy between deep water abundance and vertical mixing from Saturn Probe measurements. Alternatively, if both \( \text{CO} \) and \( \text{C}_2\text{H}_6 \) can be measured by Saturn Probe, then an independent determination of the eddy mixing from those measurements will allow comparison of the vertical dynamics from the hundreds of bars pressure level upward on the two planets. All of this depends on the ability to resolve the uncertainties in the kinetics.

5.3. Uncertainties in the kinetics

The uncertainties in the kinetics affect the constraints on both the eddy diffusion coefficient and the deep water abundance. In the planetary science community, various reaction networks have been developed for modeling many kinds of atmospheres, such as the atmosphere of Jupiter [Visscher et al., 2010], hot Jupiters (e.g., Moses et al., 2011; Venot et al., 2012; Miguel and Kaltenegger, 2014), terrestrial exoplanets (e.g., Hu and Seager, 2014) and brown dwarfs (Zahnle and Marley, 2014). These reaction networks are successful in predicting the presence of major species in the atmospheres under a wide range of temperature and pressure conditions. However, the predicted mixing ratios are subject to large errors due to the large uncertainties on individual rate coefficients in the network. As an example, the \( \text{CO}/\text{CH}_4 \) chemistry has been studied for decades (e.g., Prinn and Barshay, 1977; Yung et al., 1988; Visscher and Moses, 2011), yet some uncertainty still remains because of reaction coefficients under debate (e.g., Moses, 2014). The accuracy of most kinetic networks have yet to be tested by experiments except the one of Venot et al., 2012). The Venot et al. (2012) network is derived from one in the combustion industry and has been validated against various combustion experiments. So is this reaction network accurate in modeling the atmospheres of giant planets? One concern is that the combustion experiments are usually conducted under carbon and oxygen rich environment, however, the atmospheres of giant planets are extremely hydrogen-rich (Moses, personal communication, 2015). We investigated several other reaction networks developed in the combustion community. The reaction networks we investigated are: the “Aramco Mech v1.3” from Metcalfe et al. (2013), the “San Diego Mechanism version 20141004” (http://web.eng.ucsd.edu/mae/groups/combustion/mechanism.html), the “\( \text{C}_1\text{O}_2 \) mechanism” from Li et al. (2007); the “fort15 mech” from Sung et al. (1998); the “aaumech” from Coda Zabetta and Hupa (2008); and the “GRI-30 mech” from http://www.me.berkeley.edu/gri_mech/. All the reaction networks listed above have been validated against many combustion experiments. We applied these reaction networks to Jupiter’s atmosphere and compared the predicted CO mixing ratios in Fig. 17. The predicted CO mixing ratios do not agree with each other, especially the Venot et al. (2012) network, which is predicting a much lower value than other networks. The source of the difference is that no other networks include the channel \( \text{H} + \text{CH}_3\text{OH} \leftrightarrow \text{CH}_3 + \text{H}_2\text{O} \), which means this channel is not important for oxidation in an oxygen-rich environment. However, if this channel is indeed as fast as that measured in Hidaka...
et al. (1989) as used by the Venot et al. (2012) network, it can be crucial in determining the whole CO/CH$_4$ conversion rate. The comparison in Fig. 17 does not imply the Venot et al. (2012) network is wrong, but illustrates the point that networks validated under oxygen rich environments can give different results when applied to a hydrogen-rich environment. Ideally, networks should be tested by experiments conducted under hydrogen-rich conditions in order to improve their accuracy. In this paper, due to the unresolved uncertainties in kinetics, we considered two extreme cases for CO reaction networks. The Moses et al. (2011) reaction network represents the slowest pathway for CO destruction, while the Venot et al. (2012) model represents the fastest pathway for CO destruction. In order to have more precise predictions on CO, C$_2$H$_6$, and GeH$_4$, a few reactions need to be further investigated experimentally or theoretically to determine their rate coefficients. For a tighter CO mixing ratio prediction, the reaction rate coefficient of H + CH$_3$OH ↔ CH$_3$ + H$_2$O should be experimentally studied under conditions relevant to Jupiter and compared with the theoretical estimate by Moses et al. (2011), and the experimental estimate by Hidaka et al. (1989). For a tighter C$_2$H$_6$ mixing ratio prediction, the rate coefficient of CH$_3$ + CH$_3$ + M ↔ C$_2$H$_6$ + M under high pressure should be better determined. For a better GeH$_4$ mixing ratio prediction, the rate coefficient of GeH$_2$ + H$_2$S ↔ HGe=SH + H$_2$ should be determined. The arsenic chemistry in a hydrogen rich environment should be studied to tighten the constraints on the total As abundance.

6. Conclusions

In this paper, we used a diffusion kinetic code developed in Wang et al. (2015) to predict the abundances of various disequilibrium species on Jupiter and Saturn with updated thermodynamic and kinetic data. The dependence on the vertical eddy diffusion coefficient and the deep water abundance have been explored. We summarize our simulation results below.

- We find C$_2$H$_6$ is a useful tracer for the deep eddy diffusion coefficient. The degeneracy between high (low) eddy diffusion coefficient and high (low) deep water abundance from CO constraints can be broken by adding the constraint by C$_2$H$_6$.
- We find PH$_3$ is converted to H$_3$PO$_4$ instead of P$_2$O$_6$ as in previous studies. We identified a new chemical pathway based on a H/P/O reaction network. The PH$_3$ abundance is predicted to be insensitive to either the eddy diffusion coefficient or the deep water abundance unless $E_{H_2O}$ is higher than 20.
- We confirm that SiH$_4$ is not expected in the troposphere of either Jupiter or Saturn based on a H/Si/O reaction network. A new chemical pathway for SiH$_4$/MgSiO$_3$ (s) conversion is proposed.
- We propose a new chemical pathway for GeH$_4$ destruction. The GeH$_4$ abundance is predicted to be a sensitive function of the eddy diffusion coefficient.
- We confirm that the element As is primarily sequestered in AsH$_3$ in Jupiter and Saturn’s atmosphere by exploring a new chemical pathway for AsH$_3$ destruction.
- Since the eddy diffusion coefficient is predicted by theoretical models to be latitudinally dependent, we predict the tropospheric abundances of CO, C$_2$H$_6$, CO$_2$, and GeH$_4$ to have latitudinal variations, and the tropospheric abundances of PH$_3$ and AsH$_3$ to have no latitudinal variations.

Juno can provide multiple constraints on the eddy diffusion coefficient from its measurement of disequilibrium species by JIRAM and its measurement of the deep water abundance from the microwave radiometer. A probe with a mass spectrometer sensitive enough to detect sub-ppb level of CO and C$_2$H$_6$ can place constraints on both the deep diffusion coefficient and the deep water abundance on Saturn. A probe should be sent to equatorial latitude to maximize the probability of detecting disequilibrium species. The predictions on the disequilibrium chemistry are limited by the uncertainty in kinetics. Several reactions are worth further investigations to reduce the uncertainties and they are H + CH$_3$OH ↔ CH$_3$ + H$_2$O, CH$_3$ + CH$_3$ + M ↔ C$_2$H$_6$ + M, and GeH$_2$ + H$_2$S ↔ HGe=SH + H$_2$.
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Table 1: Observed mixing ratios of some disequilibrium species

| Species | Jupiter | Saturn |
|---------|---------|--------|
| CO      | 1.0±0.2×10^{-9} | <1.0×10^{-9} |
| PH_3    | 8±1×10^{-7} | 4±1×10^{-6} |
| SiH_4   | <2.5×10^{-9} | <2×10^{-10} |
| GeH_4   | 7±2×10^{-10} | 4±2×10^{-10} |
| AsH_3   | 2.2±1.1×10^{-10} | 3±1×10^{-9} |

Table 2: Elemental abundances used in the simulation for Jupiter and Saturn.

| Element | Jupiter | Saturn |
|---------|---------|--------|
| He      | 0.157   | 0.135  |
| C       | 2.37×10^{-3} | 5.33×10^{-3} |
| N       | 6.64×10^{-4} | 4.54×10^{-4} |
| O       | variable in the simulation | variable in the simulation |
| S       | 8.90×10^{-5} | 3.76×10^{-4} |
| P       | 7×10^{-7}   | 4×10^{-6} |
| Si      | 2.85×10^{-4} | 6.47×10^{-4} |
| Ge      | 3.93×10^{-8} | 8.93×10^{-8} |
| As      | 2.2×10^{-10} | 3.0×10^{-9} |
Figure 1: Adiabatic profiles of Jupiter and Saturn computed following the method described in Fegley and Prinn (1985).
Figure 2: Time evolution of the chemical species H, OH, C$_2$H$_6$ and NNH under constant temperature and pressure. Solid lines are computed using our code, and dashed lines are from Fig. 1 in Venot et al. (2012). The initial condition is a mixture of gas H$_2$, He, O$_2$, CH$_4$, and N$_2$ with solar elemental abundances.
Figure 3: Comparison between our model and Venot et al. (2012) model on mole fraction profiles along Saturn’s adiabat. Solid lines are from Fig. 1 in Mousis et al. (2014), which is computed using the Venot et al. (2012)’s model. Dashed lines are computed using our model. The elemental abundances we used here are $O/H = 21$ times solar, $C/H = 9$ times solar, and $K_{\text{eddy}} = 1 \times 10^9 \text{ cm}^2 \text{ s}^{-1}$, the same as those used in Fig. 1 of Mousis et al. (2014).
Figure 4: Simulation results for Jupiter using the C/N/O/H reaction network. Upper left plot is the mixing ratio of species along Jupiter’s adiabatic profile for parameters: $E_{\text{H}_2\text{O}} = 10$ and $K_{\text{eddy}} = 1 \times 10^8 \text{ cm}^2\text{s}^{-1}$ using the network A. Only species with mixing ratios $q > 1 \times 10^{-15}$ at 450 K are plotted. Upper right plot is the predicted mixing ratio of C$_2$H$_6$ as a function of $K_{\text{eddy}}$ for a range of assumed water abundances. Solid lines are calculated using network A, and dashed lines are calculated using network B. Lower plots are the predicted mixing ratio of CO and CO$_2$ as a function of the water enrichment $E_{\text{H}_2\text{O}}$ for different vertical eddy diffusion coefficient $K_{\text{eddy}}$. Solid lines are calculated using network A, and dashed lines are calculated using network B.
Figure 5: Simulation results for Saturn using the C/N/O/H reaction network. Upper left plot is the mixing ratio of species along Saturn’s adiabatic profile for parameters: \( E_{\text{H}_2\text{O}} = 10 \) and \( K_{\text{eddy}} = 1 \times 10^8 \text{ cm}^2\text{s}^{-1} \) using the network A. Only species with mixing ratios \( q > 1 \times 10^{-15} \) at 400 K are plotted. Upper right plot is the predicted mixing ratio of \( \text{C}_2\text{H}_6 \) as a function of \( K_{\text{eddy}} \) for a range of assumed water abundances. Solid lines are calculated using network A, and dashed lines are calculated using network B. Lower plots are the predicted mixing ratio of CO and \( \text{CO}_2 \) as a function of the water enrichment \( E_{\text{H}_2\text{O}} \) for different vertical eddy diffusion coefficient \( K_{\text{eddy}} \). Solid lines are calculated using network A, and dashed lines are calculated using network B.
Figure 6: Equilibrium mole fractions of phosphorus containing species along Saturn’s adiabat computed using the NASA Chemical Equilibrium Application (CEA) software. The elemental input we used are P/H = 7.8 times solar, O/H = 10 times solar, and other elemental abundances are solar except He, C, N, S, Si, Ge, and As, which are listed in table 2.
Figure 7: The predicted mixing ratio of PH$_3$ as a function of the vertical eddy diffusion coefficient $K_{\text{eddy}}$ in Jupiter’s atmosphere at a few bars level. The horizontal dashed lines show the range of observed PH$_3$ mixing ratio $q_{\text{PH}_3} = 7.0 \pm 1.0 \times 10^{-7}$ (e.g., Irwin et al., 1998). The vertical dashed lines show the range of plausible eddy diffusion coefficient.
Figure 8: The predicted mixing ratio of PH$_3$ as a function of the vertical eddy diffusion coefficient $K_{\text{eddy}}$ in Saturn’s atmosphere at a few bars level. The horizontal dashed lines show the range of observed PH$_3$ mixing ratio $q_{\text{PH}_3} = 4.0 \pm 1.0 \times 10^{-6}$ (e.g., Fletcher et al., 2011). The vertical dashed lines show the range of plausible eddy diffusion coefficient.
Figure 9: Equilibrium mole fractions of some Si-bearing species along Saturn’s adiabat computed using the NASA CEA code. The elemental input we used are Si/H = 10 time solar, O/H = 10 times solar, and other elemental abundances are solar except He, C, N, S, P, Ge, and As, which are listed in table 2.
Figure 10: Predicted mixing ratio of SiH4 as a function of the vertical eddy diffusion coefficient $K_{\text{eddy}}$ for Saturn. Different oxygen abundances are explored. Si/H = 10 times solar in the calculation.
Figure 11: Equilibrium abundances of germanium containing species along Saturn’s adiabat computed using NASA CEA code. We use Ge/H = 10 times solar, and O/H = 10 times solar. Other elemental abundances are also assumed to be solar except He, C, N, S, P, Si, and As, which are listed in table
Figure 12: Predicted mole fraction of GeH$_4$ as a function of $K_{\text{eddy}}$, the vertical eddy diffusion coefficient. The horizontal dashed lines show the range of observed mole fractions of GeH$_4$ (Bjoraker et al., 1986). The vertical dashed lines show the plausible range of $K_{\text{eddy}}$ for Jupiter. The blue dashed curves correspond to a factor of 5 uncertainty on both sides of the rate coefficient (total factor of 25).
Figure 13: Predicted mole fraction of GeH$_4$ as a function of $K_{\text{eddy}}$, the vertical eddy diffusion coefficient. The horizontal dashed line shows the observed range for $X_{\text{GeH}_4}$, which is $4 \pm 2 \times 10^{-10}$ (Noll et al., 1988). The vertical dashed lines show the plausible range of $K_{\text{eddy}}$ for Saturn. The blue dashed curves correspond to a factor of 5 uncertainty on both sides of the rate coefficient (total factor of 25).
Figure 14: The predicted mixing ratio of AsH$_3$ as a function of $K_{\text{eddy}}$, the vertical eddy diffusion coefficient. The horizontal dashed lines show the observed AsH$_3$ mixing ratio, $q_{\text{AsH}_3} = 2.2 \pm 1.1 \times 10^{-10}$ (Noll et al., 1990). The vertical dashed lines show the plausible range of $K_{\text{eddy}}$ (Wang et al., 2015). The observed abundance of AsH$_3$ corresponds to 0.3–0.8 times solar As/H ratio.
Figure 15: The predicted mixing ratio of AsH$_3$ as a function of $K_{\text{eddy}}$, the vertical eddy diffusion coefficient. The horizontal dashed lines show the observed AsH$_3$ mixing ratio, $q_{\text{AsH}_3} = 3 \pm 1 \times 10^{-9}$ (Bézard et al., 1989; Noll et al., 1989; Noll and Larson, 1991). The vertical dashed lines show the plausible range of $K_{\text{eddy}}$ (Wang et al., 2015). The observed abundance of AsH$_3$ corresponds to 5–10 times enrichment relative to solar.
Figure 16: Mole fraction of GeH$_4$ as a function of the latitude for Jupiter computed using the germanium chemical model. The horizontal profile of the vertical eddy diffusion coefficient used in the calculation is from Wang et al. (2015). The horizontal dashed lines show the average mole fractions of GeH$_4$ over longitude and over latitude between -40° and 40°, corresponding to a value of 7±2×10$^{-10}$ (Bjoraker et al. 1986).
Figure 17: Comparisons on the predicted mixing ratios of CO among various reaction networks from the combustion community. All the reaction networks shown here have been validated against many combustion experiments.

Jupiter,

\[
K_{\text{eddy}} = 1 \times 10^9 \text{cm}^2 \text{s}^{-1}
\]

\[
E_{\text{H}_2\text{O}} = 7
\]
Appendix A. Chemical pathway for CO/CH\textsubscript{4} conversion

In this appendix, we introduce our method of identifying the main chemical pathway for CO/CH\textsubscript{4} conversion. The main chemical pathway for CO/CH\textsubscript{4} conversion is automatically identified from the C/N/O/H reaction network by examining the conversion rate between different carbon bearing species using Cantera. As an example, consider the conversion between CH\textsubscript{3}O and CH\textsubscript{3}OH, a non-exhaustive list of relevant reactions are

\begin{align*}
\text{CH}_3\text{O} + \text{HCO} &\leftrightarrow \text{CH}_3\text{OH} + \text{CO}, \\
\text{CH}_3\text{O} + \text{H}_2\text{CO} &\leftrightarrow \text{CH}_3\text{OH} + \text{HCO}, \\
\text{CH}_3\text{O} + \text{CH}_3\text{O} &\leftrightarrow \text{CH}_3\text{OH} + \text{H}_2\text{CO}, \\
\text{CH}_3\text{O} + \text{CH}_2\text{OH} &\leftrightarrow \text{CH}_3\text{OH} + \text{H}_2\text{CO}, \\
\text{CH}_3\text{O} + \text{H}_2 &\leftrightarrow \text{CH}_3\text{OH} + \text{H}, \\
......
\end{align*}

The total conversion rate from CH\textsubscript{3}O to CH\textsubscript{3}OH, the inverse conversion rate, and the net conversion rate are computed by summing all the rates of each individual reactions. All pairs of carbon bearing species are considered in the computation by Cantera. Then the conversion rates are displayed with a diagram generated using a method called ReactionPathDiagram in Cantera. The conversions with rates higher than a threshold are summarized in the diagram. Specifically, we start our simulation from a mixture of Saturn composition gas under the condition of Saturn’s CO quench level (~ 900 K, 500 bars), with CO abundance slightly higher than the equilibrium abundance. The system automatically evolves to the chemical equilibrium state, and some fraction of CO is converted to CH\textsubscript{4}. This conversion process can be viewed as a flow of carbon element from CO to CH\textsubscript{4} (and other species) across the reaction network. The flow channel with the fastest rate is the main chemical pathway connecting CO and CH\textsubscript{4}. In Fig. A.18, we show two reaction path diagrams, one using the network A and the other using the network B. The net flux of element carbon from one species to another species are labeled in the diagrams. By following the path with the highest net flux from CO to CH\textsubscript{4}, we find the main chemical pathway for CO/CH\textsubscript{4} conversion as

\begin{align*}
\text{CO} + \text{H} + \text{M} &\leftrightarrow \text{HCO} + \text{M}, \\
\text{HCO} + \text{H}_2 &\leftrightarrow \text{H}_2\text{CO} + \text{H}, \\
\text{H}_2\text{CO} + \text{H} + \text{M} &\leftrightarrow \text{CH}_3\text{O} + \text{M}, \\
\text{CH}_3\text{O} + \text{H} &\leftrightarrow \text{CH}_3\text{OH} + \text{H}, \\
\text{H}_2\text{CO} + \text{H} + \text{M} &\leftrightarrow \text{CH}_2\text{OH} + \text{M}, \\
\text{CH}_2\text{OH} + \text{H}_2 &\leftrightarrow \text{CH}_3\text{OH} + \text{H}, \\
\text{CH}_3\text{OH} + \text{H} &\leftrightarrow \text{CH}_3 + \text{H}_2\text{O}, \\
\text{CH}_3\text{OH} + \text{M} &\leftrightarrow \text{CH}_3 + \text{OH} + \text{M}, \\
\text{CH}_3 + \text{H}_2 &\leftrightarrow \text{CH}_4 + \text{H}, \\
\text{CO} + 3\text{H}_2 &\leftrightarrow \text{CH}_4 + \text{H}_2\text{O}. \\
\end{align*}

The conversion from H\textsubscript{2}CO to CH\textsubscript{3}OH follows two branches. The two networks agree with each other on the main chemical pathway.

Among the chemical pathway, some steps are slower than other steps, which serves as the bottleneck of the pathway. The slowest steps among the main pathway are usually called the rate determining steps. Fast steps can reach chemical equilibrium very quickly, but the slow steps are far from equilibrium. The degree of non-equilibrium can be defined in the following way. For reactions from species A to species B, we define the forward rate as \( r_f \) and the backward rate as \( r_b \). The non-equilibrium parameter can be defined as

\[
\theta_{\text{noneq}} = \frac{(r_f - r_b)}{r_f},
\]

34
\( f_{\text{noneq}} \) is close to zero for nearly equilibrium and between zero and one for non equilibrium. In table A.3 we show the computed value of \( f_{\text{noneq}} \) for all the steps on the pathway. For the simulations using the network A, there are several steps that are far from equilibrium. Only the first step and the last step are close to equilibrium. This indicates that the steps HCO → H₂CO and H₂CO → CH₃OH have similar rate and both bottleneck the overall chemical pathway. Using a quench-level model, we find using a single rate determining step will introduce an error about 30~50% in the prediction. For the simulations using the network B, the step from CH₃OH to CH₃ is the only step far from equilibrium, therefore, it is the rate determining step. Since the network B is similar to the network in Moses et al. (2011), our findings of the rate determining step is therefore the same as the one identified by Moses et al. (2011) and Visscher and Moses (2011). The different choice of rate determining step is easy to understand. Since the network A adopted a larger reaction constant for the reaction H + CH₃OH ↔ CH₃ + H₂O, the conversion from CH₃OH to CH₃ is no not a bottleneck, and the overall rate increases.
Figure A.18: Reaction path diagram for carbon bearing species generated by Cantera. The left figure is generated using the C/N/O/H reaction network A, and the right figure is generated using the network B. The composition and temperature-pressure condition resemble the CO quench level of Saturn (∼ 900 K, 550 bars). The arrows show the flow directions of element carbon, and the labels show the net flux (in the unit of mole cm⁻³ s⁻¹) of element carbon as well as the forward flux and backward flux. The reactions responsible for the forward and backward flux are also labeled. All the carbon bearing species are considered, but only fluxes above a threshold are shown in the diagram.
Table A.3: Non-equilibrium parameter $f_{\text{noneq}}$ for reactions on the CO/CH$_4$ chemical pathway.

| reactions         | $f_{\text{noneq}}$, for network A, $t = 4\times10^4$ s | $f_{\text{noneq}}$, for network B, $t = 4\times10^6$ |
|-------------------|--------------------------------------------------------|----------------------------------------------------|
| CO → HCO          | $5.1\times10^{-4}$                                     | $1.8\times10^{-6}$                                  |
| HCO → H$_2$CO     | $9.1\times10^{-1}$                                     | $3.2\times10^{-3}$                                  |
| H$_2$CO → CH$_3$O | $4.3\times10^{-1}$                                     | $1.3\times10^{-4}$                                  |
| H$_2$CO → CH$_2$OH| $2.5\times10^{-1}$                                     | $7.8\times10^{-5}$                                  |
| CH$_3$O → CH$_2$OH| $7.6\times10^{-1}$                                     | $1.3\times10^{-4}$                                  |
| CH$_2$OH → CH$_3$OH| $8.2\times10^{-1}$                                   | $1.9\times10^{-4}$                                  |
| CH$_3$OH → CH$_3$ | $2.1\times10^{-1}$                                     | $9.5\times10^{-1}$                                  |
| CH$_3$ → CH$_4$   | $4.1\times10^{-8}$                                     | $2.5\times10^{-11}$                                 |

Appendix B. Chemical pathway for PH$_3$/H$_3$PO$_4$ conversion

The chemical pathway for PH$_3$ destruction is automatically identified by examining the conversion rate between all species in the reaction network. The method is detailed in the Appendix A using the CO/CH$_4$ conversion as an example. We start our simulation from a mixture with the Saturn-like composition: He/H = 0.27, O/H = 20 times solar, and P/H = 8 times solar. The temperature and pressure are held constant as the mixture chemically evolves to an equilibrium state. In Fig. B.19 we show the reaction path diagram for phosphorus bearing species generated using Cantera. PH$_3$ is converted to H$_3$PO$_4$ bypassing a list of species: PH$_2$, H$_3$POH, HPOH, HPO, PO, HOPO, PO$_2$, and HOPO$_2$. In table B.4 we present the computed values of $f_{\text{noneq}}$ at one instant during the chemical evolution. The only step that is far from equilibrium is the step PO$_2$ → HOPO$_2$. Therefore, the rate determining reaction for PH$_3$/H$_3$PO$_4$ conversion near the PH$_3$ quench level of Saturn is PO$_2$ + H$_2$O ↔ HOPO$_2$ + H. The rate determining step could be different if the temperature and pressure conditions were very different from 800 K and 370 bars.
Figure B.19: Reaction path diagram for phosphorus bearing species generated by Cantera. The input reaction network here is the H/P/O network described in section 3.1. The arrows in the diagram show the flow directions of element phosphorus. The labels show the net element flux (in the unit of mole cm$^{-3}$ s$^{-1}$) as well as the forward flux and the backward flux. The reactions responsible for the forward and backward flux are also labeled. All species in the network are considered, but only species that have net flux above a threshold are shown in this figure.
Table B.4: Non-equilibrium parameter $f_{\text{noneq}}$ for reactions on the PH$_3$/H$_3$PO$_4$ chemical pathway.

| reactions         | $f_{\text{noneq}}$, $t = 1 \times 10^8$ s |
|-------------------|-------------------------------------------|
| PH$_3$ $\rightarrow$ PH$_2$ | $4.7 \times 10^{-8}$ |
| PH$_2$ $\rightarrow$ H$_2$POH  | $1.5 \times 10^{-2}$ |
| H$_2$POH $\rightarrow$ HPOH   | $1.1 \times 10^{-5}$ |
| HPOH $\rightarrow$ HPO       | $3.6 \times 10^{-5}$ |
| HPO $\rightarrow$ PO         | $8.3 \times 10^{-2}$ |
| PO $\rightarrow$ HOPO        | $2.7 \times 10^{-4}$ |
| HOPO $\rightarrow$ PO$_2$    | $1.1 \times 10^{-7}$ |
| PO$_2$ $\rightarrow$ HOPO$_2$| $9.3 \times 10^{-1}$ |
| HOPO$_2$ $\rightarrow$ H$_3$PO$_4$ | $1.1 \times 10^{-8}$ |

Appendix C. Chemical pathway for SiH$_4$ destruction

Silane (SiH$_4$) is oxidized into various species in the atmosphere of Jupiter and Saturn. The major products are MgSiO$_3$ condensates. The main chemical pathway is identified following the approach detailed in the Appendix A using CO/CH$_4$ conversion as an example. We start our simulation from a mixture with a Saturn like composition: He/H = 0.27, O/H = 10 times solar, and Si/H = 10 times solar. The temperature and pressure are held constant as the mixture evolves into chemical equilibrium state. The reaction path diagram is shown in Fig. 20. The main destruction pathway of SiH$_4$ is identified from the diagram: SiH$_4$ $\rightarrow$ SiH$_2$ $\rightarrow$ HSiOH $\rightarrow$ SiO $\rightarrow$ Si(OH)$_2$ $\rightarrow$ (HOSiOOH) $\rightarrow$ HOSiO $\rightarrow$ SiO$_2$. SiO$_2$ will react with Mg(OH)$_2$ to form MgSiO$_3$ under the conditions of Jupiter and Saturn. In table we present the computed values of $f_{\text{noneq}}$ at an instant of the chemical evolution. There are three steps that are far from equilibrium. The first step is the conversion from SiH$_2$ to HSiOH, and the other two are both at the step from Si(OH)$_2$ to HOSiO. There is no unique rate-determining step for SiH$_4$ destruction.
Figure C.20: Chemical pathway for silicon bearing species generated by *Cantera*. The input reaction network here is the H/Si/O network described in section 3.1. The arrows show the flow directions of element silicon. The labels show the net flux (mole cm\(^{-3}\) s\(^{-1}\)) of element silicon as well the forward flux and the backward flux. Also labeled are the reactions responsible for the forward and backward flux. All species in the network are considered, but only species that have net flux above a threshold are shown in the diagram.
Table C.5: Non-equilibrium parameter $f_{\text{noneq}}$ for reactions on the SiH₄ destruction chemical pathway.

| reactions                      | $f_{\text{noneq}}, t = 2 \times 10^5$ s |
|--------------------------------|----------------------------------------|
| SiH₄ → SiH₂                    | $2.3 \times 10^{-4}$                   |
| SiH₂ → H₂SiOH                  | 1.0                                    |
| HSiOH → SiO                    | $9.0 \times 10^{-4}$                   |
| SiO → Si(OH)₂                  | $3.3 \times 10^{-10}$                  |
| Si(OH)₂ → HOSiO                | 1.0                                    |
| Si(OH)₂ → HSiO(OH)             | $2.9 \times 10^{-5}$                   |
| HSiO(OH) → HOSiO               | 1.0                                    |
| HOSiO → SiO₂(c)                | $1.8 \times 10^{-3}$                   |