Study on the Measurement of Stress in the Surface of Selective Laser Melting Forming Parts Based on the Critical Refraction Longitudinal Wave

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Abstract: Measurement and control of stress in the metal forming layer is the basic problem of selective laser melting (SLM) forming parts. The critical refraction longitudinal (LCR) wave method to test stress in metallic materials has been extensively studied. However, when testing of stress in selective laser melting (SLM) forming parts using this method, some deep-seated regularities of this technology are still not clear. In order to reveal the mechanism of the LCR wave method to measure stress in SLM forming parts, specimens made of 316 L stainless steel were manufactured using meander, stripe, and chessboard scanning strategies. Static load tensile test were applied to SLM forming specimens, with the purpose to demonstrate the scanning strategy has important effect on the LCR wave method to test stress in SLM forming parts. The regularity of the LCR wave velocity on stress is obtained in this study. The anisotropic microstructure of SLM forming parts has an unneglectable effect on the LCR wave stress test. The essential principle of anisotropic microstructure effecting the LCR wave velocity in SLM forming parts were revealed in the experiments. The results of the experiment provide a basis for non-destructive and reliable test of stress in SLM forming parts and other inhomogeneous materials.

Keywords: selective laser melting; stress; scanning strategy; critical refraction longitudinal (LCR) wave; anisotropic microstructure

1. Introduction

Metal powder is melted directly by a high energy laser beam when selective laser melting (SLM) technology is used to form parts layer by layer. The main problem affecting the quality of SLM parts is the selection of process parameters. The process parameters mainly include scanning strategy, scanning speed, scanning interval, layer thickness, laser power and so on [1,2]. At present, in order to ensure the quality of SLM forming parts manufactured with 316 L stainless steel, usually, a large number of specimens are prepared by orthogonal experiments or single factor experiments with different process parameters, and the optimized process parameters are selected by measuring the mechanical properties of the specimens [2–4]. In the forming process, the rapid melting/solidification rate and repeated thermal cycle result in large temperature gradient, and residual stresses easily occurs [4,5]. Present studies [5–7] show that the magnitude and distribution of residual stresses are closely related to scanning path. Residual stress seriously affects the mechanical properties of SLM forming parts [8]. The critical refraction longitudinal (LCR) wave test for stress has been extensively studied [9–11], it has the advantages of safety, nondestructiveness, and on-line detections. The method utilizing...
ultrasonic velocity [12–14] to measure stress is the focus of current research. The mechanism of the microstructure effect on the ultrasonic test result is not clear. Therefore, it is necessary to reveal the variation mechanism of ultrasonic velocity in anisotropic SLM forming parts under stress, so the ultrasonic test for stress in SLM forming parts can be done nondestructively, quickly and accurately.

Classical acoustic-elasticity theory shows that the ultrasonic velocity in material will change under the action of stress. In recent years, scholars have carried out extensive research on this technology, and achieved some significant results [12–14]. Hughes and Kelly [15] proposed the expressions of ultrasonic velocity and stress in isotropic solids based on the finite deformation theory, which laid the foundation of acoustic–elasticity theory. Johnson [16,17] deduced the acoustic–elastic formula under elastic–plastic conditions based on the elastic–plastic continuum model of Green. However, due to the obvious anisotropic microstructure of SLM forming parts and the elastic–plastic deformation of materials in the process of parts preparation, the acoustic-elasticity theory needs to be developed further.

For developing more precise and efficient ultrasonic methods to measure stress in SLM forming parts, there are two kinds of research methods at present. Firstly, the acoustic-elastic formulas suitable for the testing objects are deduced based on the theory of elastic-plastic deformation [16–18]. Secondly, the acoustic-elastic formulas that can separate or weaken tissue effects are established by experiments using specific waveforms (such as shear horizontal (SH) wave) or combination of more than two waveforms [19–21]. For example, Iwashimizu et al. [21] assumed that ultrasonic wave propagates along the direction parallel to the symmetrical axis of orthogonal materials, the effect of anisotropy was retained in the second-order elastic constants, and the effect of isotropy in third-order elastic constants was neglected. Thompson et al. [22] separated the texture effect from the stress effect by plane SH waves, whose propagation directions were perpendicular to each other. Walaszek et al. [23] used LCR method to measure the longitudinal residual stress in butt plate welding, with the results being in good agreement with that of the small hole method. These studies are useful explorations for ultrasonic nondestructive tests of stress in anisotropic materials, and have certain reference significance, but their shortcomings are also obvious. For example, most of the acoustic–elastic formulas derived from theory contain parameters such as elastic strain, plastic strain, and principal tensile rate. These complex parameters can be determined by elastic–plastic experiments. Therefore, it is difficult to popularize and apply in practice. It is necessary to develop special ultrasonic transducers for stress detection by using specific waveforms or combinations of different types of waveforms, and most of them remain at the experimental observation level, lacking in deep theoretical analysis.

The objective of this research was to explore the stress measurement mechanism of laser forming parts based on LCR wave method. For this purpose, SLM forming specimens made of 316 L stainless steel were manufactured using meander, stripe, and chessboard scanning strategies. The LCR wave method was used to test stress on the surface of SLM forming specimens. The results show that the anisotropic microstructure of SLM forming parts has an unneglectable effect on the LCR wave stress test. Inhomogeneous deformation of anisotropic SLM forming layers result in the appearance of “wave-type” fluctuations in acoustic-elastic curve during plastic deformation stage. In addition, the acoustic-elastic coefficient varies with scanning strategy, and the acoustic-elasticity equations to measure stress in SLM forming parts made of 316 L stainless steel are given in this research.

2. Acoustic-elastic Equation of LCR Wave Under Plane Stress

The principle of the LCR wave test for stress in media is shown in Figure 1. When the longitudinal wave signal is emitted by the transmitting transducer, the longitudinal wave obliquely incidents on the surface of media at the first critical angle $\theta_1$, according to Snell’s law. The LCR wave can be generated inside the medium. It propagates along the medium surface at a certain depth, the LCR wave penetration depth is related to the center frequency of the transducer [18].
Figure 1. Schematic diagram of propagation of critical refraction longitudinal (LCR) wave.

Based on the propagation characteristics of LCR wave in the medium, the definition of surface coordinates of the specimen is shown in Figure 2. LCR wave propagates on the shallow surface of the medium. On the shallow surface of the medium the restraint along its thickness direction (a3 direction) is small, and it is a free surface. Therefore, σ3 on the surface of elastic medium in a3 direction is 0. The stresses along a1 and a2 directions are respectively σ1, σ2. Therefore, the surface stress state of specimen can be simplified to plane stress state.

Figure 2. Surface coordinates of the medium.

When the LCR wave propagates along the a1 direction on the surface of isotropic medium in stress state, the plane composed of a1 and a3 vectors is defined as the displacement vector plane of the LCR wave. Based on the acoustic–elastic theory and the above coordinate definition, Husson [24] considered that the variation of ultrasonic velocity caused by stress in isotropic media can be expressed as:

\[
\frac{v_1 - v_0}{v_0} = k_1 \cdot \sigma_1 + k_2 \cdot \sigma_2
\]

(1)

\[
\frac{v_2 - v_0}{v_0} = k_2 \cdot \sigma_1 + k_1 \cdot \sigma_2
\]

(2)

where, \( v_0 \) is the velocity of LCR wave propagates in the medium under stress-free conditions. \( v_1 \) and \( v_2 \) are the velocities of LCR wave propagate along the a1 and a2 directions in the medium under stress condition, respectively. \( k_1, k_2 \) are called the acoustic–elastic coefficient, which are respectively the functions of second-order elastic constants (\( \lambda, \mu \)) and third-order elastic constants (\( l, m, n \)) of the medium [25].

It can be seen from Equations (1) and (2) that the value of stress can be calculated indirectly by measuring the variation of the LCR wave velocity propagates in the medium under stress conditions. However, it is not easy to measure the variation of the LCR wave velocity as the acoustic–elasticity effect is not obvious. Therefore, the difference in time of flight in the ultrasonic distance measurement is used to reflect the variation of the LCR wave velocity. If the distance between the transducers is \( l_0 \), the LCR wave velocity is expressed as:

\[
v_0 = \frac{l_0}{t_0}, \quad v_1 = \frac{l_0}{t_1}, \quad v_2 = \frac{l_0}{t_2}
\]

(3)

where, \( t_0 \) is the time of flight in ultrasonic distance measurement under stress-free conditions; and \( t_1 \) and \( t_2 \) are the times of flight in ultrasonic distance measurement along the a1 and a2 directions under stress conditions, respectively. Equation (3) is introduced into Equations (1) and (2) after simplification, whereby the expression between ultrasonic propagation time and stress is obtained as follows:
The propagation velocity of the LCR wave in the medium is little affected by the stress, that is, \( t_1 \approx t_2 \approx t_0 \), but \( t_0 - t_1 \neq 0 \) and \( t_0 - t_2 \neq 0 \). Therefore, Equations (4) and (5) can be simplified as follows:

\[
\frac{t_0(t_0-t_1)}{t_1} = k_1 \cdot \sigma_1 + k_2 \cdot \sigma_2 \tag{6}
\]

\[
\frac{t_0(t_0-t_2)}{t_2} = k_1 \cdot \sigma_1 + k_2 \cdot \sigma_2 \tag{7}
\]

Due to the \( t_0 \) being the reference signal, throughout the paper \( t_1 - t_0 \) and \( t_2 - t_0 \) will be used to replace \( t_0 - t_1 \) and \( t_0 - t_2 \) in Equations (6) and (7).

### 3. Experimental Procedure

#### 3.1. Specimen Preparation

316L stainless steel spherical powder was used to prepare the specimen by SLM technology. The maximum particle size of the powder is 60 \( \mu \)m and the minimum particle size is 45 \( \mu \)m, the apparent density is 4.42 g/cm\(^3\). The chemical composition of the powder is shown in Table 1. An AM400 SLM (Renishaw, Gloucestershire, West London, UK) additive manufacturing system was used in the experiment. GB/T3075-2008 [26] was used for tensile specimens. The size of the specimen is shown in Figure 3. The optimized processing parameters were selected, as shown in Table 2.

| Element | C   | Cr   | Ni   | Mo  | Si   | Mn  | O   | P   | Fe   |
|---------|-----|------|------|-----|------|-----|-----|-----|------|
| Content | 0.03| 17.5 | 12.06| 2.06| 0.86 | 0.3 | 0.1 | 0.04| Bal  |

![Table 1. Chemical compositions of 316L stainless steel spherical powder (mass fraction, %).](image)

| Laser Power (W) | Scanning Speed (mm/s) | Layer Thickness (\( \mu \)m) | Scanning Interval (mm) | Spot Diameter (\( \mu \)m) | Volume Fraction of Oxygen (%) |
|----------------|-----------------------|-----------------------------|------------------------|---------------------------|-----------------------------|
| 250            | 750                   | 30                          | 0.065                  | 80                        | 0.03                        |

![Figure 3. Schematic of tensile specimen (mm).](image)

Many scholars have studied the influence of the scanning strategy on residual stress distribution in SLM parts [3,4,27], so meander, stripe, and chessboard scanning strategies were used in the experiment for the study of stress in SLM forming parts. The scanning paths of the three scanning strategies are shown in Figures 4–6. For the three scanning strategies, the divisional direction rotation mechanism is adopted. The scan vectors are rotated by 67\(^\circ\) between sub-areas of the adjacent two layers.
With a linear scanning vector, as shown in Figure 4a. The scanning lines belonging to the same layer were parallel to each other and are perpendicular to the boundaries of the two adjacent sub-areas. The length of the scan vector is limited by the width of the rectangle sub-area. As shown in Figure 5a, the sub-areas are scanned successively in the order of down to top, left to right.

For the stripe scanning strategy, the cross section is divided into isometrical rectangle sub-areas allowing a small amount of overlap between the two adjacent rectangle sub-areas in the same layer. The overlap area was 0.08 mm which was equal to the spot diameter in the experiment. The stripe scanning lines follow the rules that the orientations of the scan vectors in the same layer, and the sub-areas with the same scan vectors are successively scanned first before the sub-areas with different scan vectors in the same line. The length of the scan vector is limited by the width of the rectangle sub-area. As shown in Figure 5a, the sub-areas are scanned successively in the order of down to top, left to right.

When the meander scanning strategy is adopted, the cross section of the forming part is filled with a linear scanning vector, as shown in Figure 4a. The scanning lines belonging to the same layer are parallel to each other. The orientations of the two adjacent scan vectors are opposite. When the scanning interval is set to 0.065 mm, which is less than the spot diameter (0.08 mm), the compactness of the SLM forming part can be ensured.

For the chessboard scanning strategy, a literal chessboard style is followed, the cross section is divided into isometrical rectangle sub-areas allowing a small amount of overlap between the two adjacent rectangle sub-areas in the same layer. The overlap area was 0.08 mm which was equal to the spot diameter in the experiment. As shown in Figure 6a, the sub-areas are scanned line by line, according to their order of arrangement in the same layer, and the sub-areas with the same scan vectors are successively scanned first before the sub-areas with different scan vectors in the same line. The length of the scan vector is equal to the width of the square sub-area. The width of the sub-area is suitable for the choice of...
Therefore, the area width selected in the experiment is 5 mm. Three kinds of specimens manufactured using meander, stripe, and chessboard scanning strategies are manufactured. Five specimens for each scanning strategy are manufactured, and the processing parameters shown in Table 2 are used during specimen preparation.

### 3.2. Experimental System

The ultrasonic test system is shown in Figure 7. The Panametrics-NDT 5800PR ultrasonic pulse transmitting instrument (Waltham, MA, USA), and the TDS5000B oscilloscope with 2.5 GHz sampling frequency (Tektronix, Beaverlon, OR, USA) were used in the experiment. A transmitting transducer and a receiving transducer (SIUI, Shantou, China) with diameter of 6 mm and 5 MHz center frequency were used for transmitting and receiving signals. The distance between the two transducers was 25 mm. The bandwidth of the transducer was 2.5–7.5 MHz. The transducer and the acoustic wedge were fixed together. Prior to applying the TM-100 medical ultrasonic couplant (Xiyuan temple, Tianjin, China) to the acoustic wedge and the surface of the specimen, the surface of the specimen was wiped to keep the contact surface completely clean. Then the specimen and the transducer were wound with an elastic band, to ensure the fixed position of the transducer was stable during the experiment. The testing temperature was 25 °C. The computer worked with the ultrasonic test set-up for signal acquisition and processing.

![Figure 7. Ultrasonic test system for signal generation and acquisition.](image)

The specimens were annealed for acquiring the zero-stress state. The time of flight $t_{i0}$ ($i = 1, 2$, represents the LCR wave propagation direction) in ultrasonic distance measurement (25 mm) in the surface of the specimen were recorded as reference signals. The received time domain signals for the specimens (manufactured using meander scanning strategy) under the zero-stress state are shown in Figure 8. In order to measure the time of flight $t_i$ ($i = 1, 2$) in ultrasonic distance measurement in the surface of the specimen under different stress states, the tensile testing of the specimen was carried out on the WDW-200E universal testing machine (Youdao Material Testing Machine Co., Ltd., Jinan, China). Five specimens for each scanning strategy were tested. During the experiment, the specimens were tested under the load from zero to fracture. The load interval was 2 KN, and it was slowly loaded to the predetermined load at the loading speed of 1KN/s. The loading direction and the LCR wave propagation direction are shown in Figure 9. Five times of data were collected along the $a_1$ and $a_2$ directions under each load.
when the stress damage of the SLM forming parts reaches the plastic deformation level, which are no longer met the basic requirements of servicing conditions, it is not necessary to fit the acoustic–elastic curves in the $a_1$ and $a_2$ directions can be divided into two parts: linear and non-linear. The stresses at the turning point of the curves are called critical stress. The specimens were being elastic deformation when the stress was less than the critical stress. The acoustic time difference varied linearly with the stress, which is consistent with the results expressed by Equations (6) and (7). There was a positive linear relation in the $a_1$ direction, and a negative linear relation in the $a_2$ direction. The specimens were being plastic deformation when the stress was greater than the critical stress. In practical applications, when the stress damage of the SLM forming parts reaches the plastic deformation level, which are no longer met the basic requirements of servicing conditions, it is not necessary to fit the acoustic–elastic curves at this stage. The linear part of acoustic-elastic curves in the $a_1$ and $a_2$ directions were fitted by the least square method [30] based on the criterion of a high correlation coefficient and small standard deviation [30,31]. Figure 13a,b show the Linear fitting results, and Equations (8)–(10) show the fitting results. Figure 13a,b are plotted according to the average value of the test results, where the critical stress values of the three kinds of specimens are 371 MPa, 474 MPa, and 492 MPa. The relevant statistical data is shown in Table 3. $k_1$ and $k_2$ are the linear fitting coefficients in $a_1$ and $a_2$ directions, respectively. As shown in Table 3, the standard deviations are very small; therefore the test results are reliable.

4. Experimental Results

4.1. Calibration of the Acoustic–Elastic Coefficient

Three kinds of specimens were tested according to the configuration described above. The signal collected under the zero-stress state was used as reference signal, and the signal collected under different stress states was used as the testing signal. Acoustic time difference ($\Delta t_i = t_i - t_i^0$, $i = 1, 2$) between the testing signal and the reference signal was determined by the cross correlation method [29]. The test results are shown in Figures 10–12. As can been seen from the figures, the acoustic-elastic curves in the $a_1$ and $a_2$ directions can be divided into two parts: linear and non-linear. The stresses at the turning point of the curves are called critical stress. The specimens were being elastic deformation when the stress was less than the critical stress. The acoustic time difference varied linearly with the stress, which is consistent with the results expressed by Equations (6) and (7). There was a positive linear relation in the $a_1$ direction, and a negative linear relation in the $a_2$ direction. The specimens were being plastic deformation when the stress was greater than the critical stress. In practical applications, when the stress damage of the SLM forming parts reaches the plastic deformation level, which are no longer met the basic requirements of servicing conditions, it is not necessary to fit the acoustic–elastic curves at this stage. The linear part of acoustic-elastic curves in the $a_1$ and $a_2$ directions were fitted by the least square method [30] based on the criterion of a high correlation coefficient and small standard deviation [30,31]. Figure 13a,b show the Linear fitting results, and Equations (8)–(10) show the fitting results. Figure 13a,b are plotted according to the average value of the test results, where the critical stress values of the three kinds of specimens are 371 MPa, 474 MPa, and 492 MPa. The relevant statistical data is shown in Table 3. $k_1$ and $k_2$ are the linear fitting coefficients in $a_1$ and $a_2$ directions, respectively. As shown in Table 3, the standard deviations are very small; therefore the test results are reliable.
Meander scanning: \[
\begin{align*}
\Delta t_1 &= 0.0781\sigma_1 - 2.559 \\
\Delta t_2 &= -0.0258\sigma_1 - 0.912
\end{align*}
\] (8)

Stripe scanning: \[
\begin{align*}
\Delta t_1 &= 0.0566\sigma_1 - 0.885 \\
\Delta t_2 &= -0.0206\sigma_1 - 0.523
\end{align*}
\] (9)

Chess board scanning: \[
\begin{align*}
\Delta t_1 &= 0.0544\sigma_1 + 1.783 \\
\Delta t_2 &= -0.0191\sigma_1 + 0.505
\end{align*}
\] (10)

**Figure 10.** Ultrasonic testing results of the specimens manufactured using meander scanning strategy. (a) $a_1$ direction; (b) $a_2$ direction.

**Figure 11.** Ultrasonic testing results of the specimens manufactured using stripe scanning strategy. (a) $a_1$ direction; (b) $a_2$ direction.

**Figure 12.** Ultrasonic testing results of the specimens manufactured using chessboard scanning strategy. (a) $a_1$ direction; (b) $a_2$ direction.
4.2. Analysis of Linear Part in Acoustic-Elastic Curves

As shown in Figure 13, when the stress is less than the critical stress, the acoustic time difference varied linearly with the stress. According to Equations (8)–(10), the elastic coefficients in a_{1} direction are 0.0781 ns MPa\(^{-1}\), 0.0566 ns MPa\(^{-1}\), and 0.0544 ns MPa\(^{-1}\). The acoustic-elastic coefficients in a_{2} direction are −0.0258 ns MPa\(^{-1}\), −0.0206 ns MPa\(^{-1}\), and −0.0191 ns MPa\(^{-1}\). Thus, it can be seen that in the same specimen, the acoustic-elastic coefficient parallel to the LCR wave propagation direction is about three times that than perpendicular to LCR wave propagation direction. The acoustic-elastic coefficients and constant terms vary with the specimens manufactured using different scanning strategies, as the mechanical properties and microstructures of the specimens are different. The stress-strain curves of the three kinds of specimens are shown in Figures 14–16, and tensile properties parameters of the specimens manufactured using meander, stripe, and chessboard scanning strategies are shown in Table 4 (the three kinds of specimens are marked as A, B, C). This indicates that tensile strength, yield strength, elastic modulus, and the maximum strain of the SLM forming parts vary with the scanning strategy, and the differences of tensile properties of the same type of specimen are small. Reasonable
sub-area and staggered scanning sequences can significantly improve the tensile properties of the SLM specimens. The experiment results show that the better the tensile properties of the specimens are, the smaller the absolute values of the acoustic–elastic coefficients in the same direction are. As shown in Figure 17a–c, the variety of defects, such as inclusions and micro-holes, inevitably exist in the SLM forming specimens. Obviously, there are more defects existing in the specimen whose tensile properties are worse. Thus, under the action of stress, specimens with more defects are more likely to deform, therefore the change rate of the propagation velocity of the LCR wave is larger and the absolute value of the corresponding acoustic–elastic coefficients are also larger, which is consistent with the test results.

Figure 14. Stress-strain curves of the specimens manufactured using meander scanning strategy. (a) Stress-strain curves. (b) Local enlarged drawing of stress-strain curves.

Figure 15. Stress-strain curves of the specimens manufactured using stripe scanning strategy. (a) Stress-strain curves. (b) Local enlarged drawing of stress-strain curves.

Figure 16. Stress-strain curves of the specimens manufactured using chessboard scanning strategies. (a) Stress-strain curves. (b) Local enlarged drawing of stress-strain curves.
Table 4. Tensile properties of SLM specimens under different scanning strategies.

| Specimen Number | Tensile Strength (MPa) | Yield Strength (MPa) | Elastic Modulus (N/mm²) | The Maximum Strain (%) |
|-----------------|------------------------|----------------------|-------------------------|------------------------|
| A-1             | 528                    | 465                  | 114,007                 | 17.4                   |
| A-2             | 530                    | 470                  | 115,092                 | 18.4                   |
| A-3             | 534                    | 472                  | 116,489                 | 17.6                   |
| A-4             | 516                    | 450                  | 114,023                 | 18.0                   |
| A-5             | 518                    | 453                  | 114,143                 | 17.0                   |
| Mean            | 525.20                 | 462.00               | 114,750                 | 17.68                  |
| Standard deviation | 7.82                  | 9.98                 | 1071.20                 | 0.54                   |

| Specimen Number | Tensile Strength (MPa) | Yield Strength (MPa) | Elastic Modulus (N/mm²) | The Maximum Strain (%) |
|-----------------|------------------------|----------------------|-------------------------|------------------------|
| B-1             | 620                    | 532                  | 151,064                 | 29.5                   |
| B-2             | 611                    | 528                  | 151,792                 | 28.5                   |
| B-3             | 590                    | 522                  | 154,266                 | 27.3                   |
| B-4             | 595                    | 513                  | 154,764                 | 28.4                   |
| B-5             | 604                    | 520                  | 151,357                 | 27.8                   |
| Mean            | 604.00                 | 520.80               | 152,650                 | 28.30                  |
| Standard deviation | 12.06                 | 5.63                 | 1732.50                 | 0.82                   |

| Specimen Number | Tensile Strength (MPa) | Yield Strength (MPa) | Elastic Modulus (N/mm²) | The Maximum Strain (%) |
|-----------------|------------------------|----------------------|-------------------------|------------------------|
| C-1             | 629                    | 532                  | 177,896                 | 32.2                   |
| C-2             | 635                    | 534                  | 177,665                 | 35.6                   |
| C-3             | 646                    | 550                  | 176,953                 | 34.6                   |
| C-4             | 620                    | 526                  | 177,562                 | 35.0                   |
| C-5             | 640                    | 528                  | 176,356                 | 32.8                   |
| Mean            | 634.00                 | 534.00               | 177,290                 | 34.24                  |
| Standard deviation | 10.02                 | 9.48                 | 626.04                  | 1.19                   |

Figure 17 shows the microscopic fracture morphology of tensile specimens. As can be seen from the Figure 17, all the specimens exhibited ductile fracture with dimples. The fracture surfaces show obvious dimple characteristics and good plasticity macroscopically. As shown in Figure 17a–c, there are many micro-holes on the surface of the fracture, and many micro-holes are formed by inclusion fragmentation. Under the action of stress, these voids grow continuously, and aggregate to form dimples and large voids. 316 L stainless steel is sensitive to voids. Voids accumulate and eventually lead to the fracture of the specimen. Its fracture mechanism is dimple-micropore aggregation.

Figure 17. Microscopic fracture morphology of tensile specimens. (a) Meander scanning strategy. (b) Stripe scanning strategy. (c) Chess board scanning.
Stress-strain curves in Figures 14–16 show that the tensile properties of the specimens vary with the scanning strategies, however, the tensile process can all be divided into elastic deformation and plastic deformation stages. The stress at the turning point of the acoustic-elastic curve is less than the yield stress at the stress-strain curve. Based on the acoustic-elastic theory and the microstructural analysis of the specimens, the causes of this phenomenon are analyzed. Figure 18 shows the microstructures of the specimens. Microstructures of 316 L stainless steel specimens manufactured by SLM technology mainly consists of columnar, cellular, and equiaxed crystals. Specimens were prepared by multi-channel overlapping and multi-layer stacking, therefore there are arc-shaped fusion interfaces within the microstructure. The formation of columnar and cellular crystals in the microstructure are due to the large temperature gradient during SLM forming, which is a process of rapid heating and cooling, and this rapid change of temperature promotes the formation of columnar and cellular crystals [32,33]. In the same molten pool, the growth direction of columnar and cellular crystals is perpendicular or at a certain angle to the fusion interface, which shows that 316 L stainless steel specimens manufactured by SLM technology have obvious anisotropic characteristics. Therefore, when the specimen is subjected to tensile loading, the fusion interfaces and anisotropic structure will lead to uneven deformation in different sub-areas of the specimen. When the stress is greater than critical stress, the deformation of some sub-areas (fusion interfaces, defects, columnar and cellular crystal boundaries, etc.) are larger than other sub-areas (equiaxed crystal areas). Therefore the areas with large deformations first enter the plastic deformation stage, and meanwhile the areas with small deformations are still in the elastic deformation stage, the higher the stress is, the larger the plastic deformation area is. The “average deformation” of the specimen in ultrasonic distance measurement has entered the plastic deformation stage, therefore the variation law of the LCR wave signal varies with stress no longer conforming to the linear law, however, the specimen hasn’t entered the plastic deformation stage. When the stress has increased to yield stress, the plastic deformation region is extended to the whole specimen, and the specimen enters the plastic deformation stage.

Figure 18. Microstructures of SLM specimens. (a) Meander scanning strategy. (b) Stripe scanning strategy. (c) Chess board scanning strategy.
4.3. Analysis of Non-Linear Parts in Acoustic-Elastic Curves

As shown in Figure 13, when the stress is greater than the critical stress, the acoustic–elastic curves appear a style of wave trend. Experiment results show that the SLM forming specimens manufactured with 316 L stainless steel have a good plastic deformation ability in the static tension process. Plastic deformation is the main factor affecting the fluctuation of non-linear parts in acoustic–elastic curves. Therefore, the variation rule of the acoustic–elastic curves within this stress range is theoretically analyzed based on the theory of metal plastic deformation. Plastic deformation of metal is achieved by dislocation motion [34]. Dislocations include as-grown dislocations and induced dislocations. As-grown dislocations are defects in crystals. Induced dislocations are formed by the adjustment of lattice structure when crystals are subjected to stress. Under the action of stress, the dislocations move along the direction of Bernard vectors on the slip surface [35,36]. As shown in Figure 18, the microstructures of SLM specimens show obvious anisotropic characteristics. Directional growth of columnar, cellular grain boundaries, and fusion interfaces are obstacles to dislocation movement. When the force driving the forward movement of dislocations cannot overcome the resistance of the obstacles, dislocation pile-up group will occur. With the increase of the number of dislocations in the pile-up group, the stress in the local region increases gradually. As the fracture mechanism of the specimen is dimple-micropore aggregation, the stress concentration produced by dislocation pile-up cannot be released by plastic deformation. When the dislocation pile-up stress reaches the crystal fracture strength, cracks will appear in the crystals. When the stress σc is smaller than the critical state, the crack begins to propagate and the stress is released with the propagation of cracks, and the propagation velocity of the LCR wave in the surface of SLM specimen increases gradually, so the acoustic–elastic curves in Figure 10a fluctuates downward. Similarly, when the LCR wave propagates along the direction perpendicular to the tensile load, with the concentration–release-concentration of the stress in specimen, the non-linear part of the acoustic-elastic curves in Figure 10b fluctuates downward–upward–downward. When the crack extends to a new length, according to Equation (12), with the increase of crack size, only the new critical state is satisfied can the crack reach the condition of unstable propagation, and the crack is in a temporary stable state. With the increase of stress, the new critical state of crack propagation is satisfied, and the crack continues to expand. With the instability

\[
K = Y\sigma \sqrt{a} \tag{11}
\]

where \(Y\) is the shape factor of the crack, which is a dimensionless coefficient; \(\sigma\) is the mean stress (MPa); and \(a\) is half-length of crack (mm). Equation (11) shows that when the crack is in the critical state of propagation, the stress field intensity factor can be expressed as \(K_c\):

\[
K_c = Y\sigma_c \sqrt{a_c} \tag{12}
\]

where \(\sigma_c\) is the mean stress in critical state (MPa); and \(a_c\) is the half-length of crack in critical state (mm). According to the theory of crack propagation, \(K > K_c\) is the necessary condition for the unstable propagation of crack. The crack size expands continuously through the propagation. The aggregation of adjacent microcracks results in visible microvoids. Under the action of continuous stress, the microvoids grow and proliferate gradually until the specimen breaks. For 316 L stainless steel SLM specimens, when the LCR wave propagates along the direction parallel to the tensile load and the stress \(\sigma < \sigma_c\), the crack does not propagate, the stress at the crack tip increases gradually with the increase of stress, and thus the propagation velocity of the LCR wave in the surface of SLM specimen decreases gradually. Therefore the acoustic time difference increases and the non-linear part of acoustic-elastic curves in Figure 10a fluctuate upward. When the stress \(\sigma > \sigma_c\), the crack begins to propagate and the stress is released with the propagation of cracks, and the propagation velocity of the LCR wave in the surface of SLM specimen increases gradually, so the acoustic time difference decreases and the acoustic-elastic curves in Figure 10a fluctuates downward. Similarly, when the LCR wave propagates along the direction perpendicular to the tensile load, with the concentration–release-concentration of the stress in specimen, the non-linear part of the acoustic-elastic curves in Figure 10b fluctuates downward–upward–downward. When the crack extends to a new length, according to Equation (12), with the increase of crack size, only the new critical state is satisfied can the crack reach the condition of unstable propagation, and the crack is in a temporary stable state. With the increase of stress, the new critical state of crack propagation is satisfied, and the crack continues to expand. With the instability
of crack propagation in the specimen, the stress concentration–release–concentration process occurs. Therefore, when the stress reaches critical value, with the increase of stress, the acoustic–elastic curves in SLM specimens appear a style of wave trend.

The above theoretical analysis was validated by the ultrasonic microscopic imaging method [39]. The defects imaging was realized by analyzing and comparing the intensity of reflected signal, and the imaging results have the characteristics of high definition and strong contrast [40]. As shown in Figure 19, the ultrasonic microscope testing equipment VUE 250-P (OKOS, Manassas, VA, USA) was used in the experiment. The SLM specimens manufactured using stripe scanning strategy were imaged. The stress states of the tested specimens were 20 MPa and 400 MPa. The central frequency of the longitudinal wave signal was chosen as 100 MHz, and the sampling rate recording the receiving signals was set to 110 MHz. According to the loading mode of the specimen, the specimens were scanned globally along the path parallel to the loading direction. The scanning path and results are shown in Figure 20.

Figure 19. VUE250-P Ultrasonic microscope testing equipment.

(a) (b) (c)

Figure 20. The scanning path and ultrasonic microscopic imaging results of the specimens. (a) Scanning path of ultrasonic microscopic imaging. (b) Scanning imaging result of specimen (20 MPa). (c) Scanning imaging result of specimen (400 MPa).

It can be seen from Figure 20 that the imaging results of specimen (stress state is 20 MPa) are basically uniform in color distribution, and that “stripe” areas with uneven color appear in the imaging results of the specimen (stress state is 400 MPa). According to the principle of ultrasonic microscopic imaging, the large difference of color brightness in imaging results indicates a large defect size in the tested specimen, and vice versa. The imaging results show that there were several small cracks that had emerged in the specimen (stress state is 400 MPa), however, there were few cracks in the specimen (stress state is 20 MPa), which is basically consistent with the results of the aforementioned mentioned theory analysis.
4.4. Acoustic-Elastic Equations for Testing Stress in 316 L Stainless Steel SLM Parts

When the LCR wave method is used to test stress in SLM forming parts, the time of flight \( t \) in ultrasonic distance measurement in the surface of the part can be expressed as \([41,42]\):

\[
t = t_0 + \Delta t_T + \Delta t_M + \Delta t_S + \Delta t_R + \Delta t_C
\]  
(13)

where \( t_0 \) is the time of flight in ultrasonic distance measurement when the part is homogeneous, isotropic and stress-free; and \( \Delta t_T \), \( \Delta t_M \), \( \Delta t_S \), \( \Delta t_R \), and \( \Delta t_C \) are the influences of temperature, microstructure, stress, surface roughness, and coupling mode, on the time of flight, respectively.

In the actual testing process, when the temperature, surface roughness and coupling mode remain unchanged, the acoustic time difference is \( \Delta t = t_i - t_i^0 = \Delta t_M + \Delta t_S \), so as shown in Equations (8)–(10), the acoustic time difference varied linearly with the stress. The constant terms in Equations (8)–(10) indicate the acoustic time difference is caused by the microstructure of material. As shown in Figure 18, 316 L stainless steel specimens manufactured by SLM technology have obvious anisotropic characteristics, and the microstructures vary with the change of the fixed positions of the transducers in the specimen manufactured using the same scanning strategy. According to the ultrasonic propagation theory, due to the influence of the anisotropic tissue effect, the ultrasonic longitudinal wave appears to be a complex physical phenomenon such as beam deflection and focusing in the process of propagation \([43,44]\). In order to evaluate the effect of anisotropic structures on testing results objectively, the SLM specimen was prepared with the same process parameters (meander scanning strategy was adopted), and the specimen was annealed. Using the same detection method as described above, the LCR wave signals at four different positions on the surface of the specimen were collected, and the results are shown in Figure 21. When the specimen is in stress-free state, the time of flight of the LCR wave signal propagating along the same direction in the fixed ultrasonic path (25 mm) is not the same, the average variation is 2.43 ns, the constant term in acoustic–elastic Equation (8) is 2.559, and there is no significant difference between them. Therefore, it can be considered that the constant terms in Equations (8)–(10) indicate the acoustic time difference is caused by the microstructure of material.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{received_signals.png}
\caption{The received time domain signals corresponding to different detection positions. (a) Detection positions. (b) The received time domain signals.}
\end{figure}

Therefore, the acoustic–elastic equations for testing stress in 316 L stainless steel SLM parts are as follows:

\begin{align*}
\text{Meander scanning :} & \quad \begin{cases} 
\Delta t_1 = 0.0781\sigma_1 - 0.0258\sigma_2 - 2.559 \\
\Delta t_2 = -0.0258\sigma_1 + 0.0781\sigma_2 - 0.912 
\end{cases}
\end{align*}

(14)
stripe scanning:
\[
\Delta t_1 = 0.0566\sigma_1 - 0.0206\sigma_1 - 0.885
\]
\[
\Delta t_2 = -0.0206\sigma_1 + 0.0566\sigma_1 - 0.523
\]

(15)

\[
\Delta t_1 = 0.0544\sigma_1 - 0.0191\sigma_2 + 1.783
\]
\[
\Delta t_2 = -0.0191\sigma_1 + 0.0544\sigma_2 + 0.505
\]

(16)

where $\Delta t_1$ and $\Delta t_2$ are the acoustic time difference in ultrasonic distance measurement along the directions perpendicular to each other; and $\sigma_1$ and $\sigma_2$ are the stresses corresponding to the detection directions.

5. Discussion

The experimental results reported in this paper enable us to understand more accurately the mechanism of the LCR wave method to measure stress in selective laser melting forming parts. According to the change rule of acoustic-elastic curve, the fracture mechanism of SLM forming parts under stress can be analyzed. The acoustic-elastic equations obtained in the experiments can be used to test stress in 316 L stainless steel SLM parts.

For SLM forming parts manufactured with 316 L stainless steel, the acoustic-elastic coefficient varies with the scanning strategy used in the forming process. For the same SLM forming parts, the acoustic-elastic coefficient parallel to the LCR wave propagation direction is about three times that of perpendicular to the LCR wave propagation direction, which is consistent with existing research [10]. Figures 10–12 show the ultrasonic testing results of the three kinds of specimens manufactured using meander, stripe, and chess board scanning strategies respectively. The change rules of acoustic–elastic curves are closely related to the stress-strain characteristics of the specimen. The stress-strain characteristics of the specimen are determined by the mechanical properties and microstructure of the material. To further confirm the scanning strategy has an important effect on the mechanical properties of SLM forming specimens, the microstructure and properties of the specimens are characterized by SEM and static tensile tests. Figures 14–16 show that the scanning strategy can significantly affect the mechanical properties of the SLM forming parts. Reasonable sub-area and staggered scanning sequences can improve the mechanical properties of the SLM specimens. Figure 18 shows 316 L stainless steel specimens manufactured by SLM technology have obvious anisotropic characteristics. Therefore, when the specimen is subjected to tensile loading, the deformation of the specimen is not uniform. This leads to the stress at the turning point of acoustic–elastic curve being less than the yield stress at the stress-strain curve. Figure 17 shows there are more defects existing in the specimen whose mechanical properties are worse, so the specimens with more defects are more likely to deform under the action of stress, therefore the absolute values of the corresponding acoustic-elastic coefficients are also larger.

We also analyzed the variation law of the acoustic–elastic curve combined with acoustic–elasticity theory and the microstructure of the specimens. It can be observed (Figure 20) that when the stress is 400 MPa, many small cracks emerge inside the specimen. The crack size expands continuously through the propagation, which results in the acoustic-elastic curves appearing a style of wave trend.

6. Conclusions

In this paper, the LCR wave method was used to explore the regularity of the dependence of acoustic time difference in ultrasonic distance measurement on the stress in SLM forming parts. For the purpose, an effective testing system was established and the corresponding tests were carried out in this study.

- It demonstrates that the absolute values of the acoustic–elastic coefficients show a significant dependence on the scanning strategies used in the SLM forming process, and the mechanical properties of the specimen vary with the scanning strategy [27,45]. For the specimen whose mechanical properties are better, the absolute values of the corresponding acoustic-elastic coefficients were less.
• The test results reveal that when the stress in an anisotropic SLM specimen is greater than critical stress and less than yield stress, many small cracks emerge inside the specimen. This indicates the specimen has entered the failure stage. This phenomenon reflects the sensibility of this method.

• As the 316 L stainless steel specimens manufactured by SLM technology present obvious anisotropic characteristics, the time of flight in ultrasonic distance measurement along the detection direction will be influenced by the anisotropic tissue. Generally, acoustic time difference in ultrasonic distance measurement keeps at nanosecond level, even if the influence of the anisotropic tissue on the acoustic time difference is very small, the influence on the reliability of stress detection results cannot be ignored. As shown in Equations (14)–(16), due to the acoustic-elastic coefficient being very small, the small fluctuation of acoustic time difference can lead to remarkable change in stress testing results. The test results indicate that the influence of anisotropic tissue on the test results can be characterized by the constant term in the linear acoustic-elastic formula, when other influencing factors in the experiment are excluded. Therefore when the LCR wave method is used to test stress, the influence of anisotropic tissue should be considered in characterizing stress in SLM forming parts.

• In any case, the sensibility of the LCR wave method to test stress has been widely proven and the robustness and stability will be particularly important in further research.

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