Adaptive fixed-time control for nonlinear systems against time-varying actuator faults

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Abstract The adaptive fixed-time control problem for nonlinear systems with time-varying actuator faults is investigated in this paper. A novel adaptive fixed-time controller is designed via combining the Lyapunov stability theory with the backstepping method. It can be adapted to both system uncertainties and unknown actuator faults. Compared with the existing fault-tolerant control schemes subject to actuator faults, the adaptive fixed-time neural networks control scheme can make sure that the tracking error is convergent in a small neighborhood of the origin within a fixed-time interval, and it does not depend on the original states of the system and actuator faults. In light of the control scheme proposed in this paper, the fixed-time stability of the closed-loop system can be guaranteed by theoretical analysis, and a numerical example is provided to verify the effectiveness of obtained theoretical results.

Keywords Uncertain nonlinear systems · Backstepping method · Unknown actuator faults · Adaptive fixed-time control

1 Introduction

In most practical control systems, sensor, actuator and the plant itself faults may occur at uncertain time, which can lead to poor performance and even instability of control systems. Therefore, it is significant to improve system reliability and safety not only by designing fault tolerant control (FTC) to compensate the effect caused by faults automatically, but also by enhancing reliability of signal components. In recent years, FTC of nonlinear systems has received extensive attention, and application examples of nonlinear systems include automotive suspensions [1], jet engine stall and surge control [2], aircraft wing rock control [3], induction motors [4] and so on. The approaches of the FTC design can be broadly divided into two categories: the passive one [5–7] and the active one [8–10]. Although the passive approach is usually exploited to handle partial actuator faults [11] and complete actuator faults [12], it
has also a limited capability of handling unknown actuator faults due to its passive control laws being fixed. Different from passive approaches, active ones consist in reconstructing the controller online, which are more capable of coping with unknown actuator faults. Based on existing results, a mass of active approaches are designed online by employing different approaches, such as adaptive method [13], sliding mode control method [14,15] and fuzzy control method [16].

In particular, among active methods, it seems that the adaptive control method is a most representative solution. For example, an adaptive FTC was presented for unknown uncertain systems (UNSs) in [17] where the fault-tolerant capacity was enhanced by applying adaptive bounding design techniques. However, in [17], the system uncertainty needs to meet the matching conditions, which is not easy to achieve in the practical system. Therefore, based on the demand of the constraint of the system uncertainty meeting the matching condition being released, the backstepping method is introduced into adaptive FTC. Since backstepping approaches were proposed, they were been widely used to design adaptive FTC for UNSs in [18] and [19]. For instance, in [20], based on the backstepping technique, adaptive FTC approaches were designed to handle actuator faults in nonlinear systems where the FTC method runs through the entire backstepping control when there exist actuator faults and guarantee tracking precision. Identically, in [21], the combination of backstepping approaches and adaptive FTC with UNSs greatly also improves the system stability and accuracy. However, the analysis of FTC is usually at infinite time; namely, FTC is able to ensure the system performance of the origin when time tends to infinity. Obviously, during a highly critical mission, such the infinite time may not be an optimal option. Actually, in finite time [22–24], that the tracking error is convergent is always required even when faults occur. After learning sufficient literature, finite-time Lyapunov stability was first presented in [25]. Up to now, abundant results have been obtained under the circumstance of nonlinear systems [26–29]. Based on FTC stability, [30] and [31] obtained some interesting results in regard to finite-time FTC with actuator faults. Specifically, the finite-time FTC for UNSs against actuator faults was investigated in [30] by neural networks (NNs) and fuzzy logic systems. It is worth noting that most results including actuator faults only involve bias faults, not gain faults. In practical operation, the abrupt faults which cover bias faults and gain faults are very difficult to avoid. With the development of modern control theory, [31] was devoted to handling the finite-time FTC problem of UNSs with such faults. In addition, adaptive finite-time fuzzy tracking control with bias and gain faults was considered in [32] for UNSs. Although there exist a mass of studies on tracking control, there is a restriction in the existing literature on finite-time tracking control of UNSs, that is, the designed finite-time control laws might not satisfy the demand of some applications because of depending on the initial conditions.

Due to the harsh external environment, the initial conditions of the system may not be known. To deal with the unknown initial conditions of finite-time control problems, the fixed-time stability was first proposed by Polyakov in [42], in which it estimated the settling time, and it is independent on the initial conditions which is confirmed in [33]. Recently, a mass of research results on the fixed time have been achieved for first-order dynamic systems [34] and second-order dynamic systems [35]. In the case of specific spacecraft saturation and actuator fault [36], a fixed-time adaptive control method was proposed to solve the singularity problem based on switched nonlinear systems. In [37], the problem of spacecraft encounter and mooring of freely rotating targets was solved. The adaptive fixed-time controller is designed to ensure the fixed-time uniformly ultimate boundedness of the tracking errors when there exist external faults and engine faults. However, there exists little literature for higher-order dynamic systems. Inspired by this, a high-order dynamic non-strict feedback system is adopted in this paper. However, due to existing uncertainties, a traditional form of fixed-time stability convergence is hard to obtain. To solve this dilemma, lots of adaptive FTC are introduced into existing research by using radial basis function neural networks (RBFNNs) [38]. However, in the above results of FTC, most schemes focus on the finite-time stability. In [39], within a finite time interval, a class of UNSs is able to track the reference signal suffering from both bias faults and gain faults. The gain which has time-varying form and uncertain bias faults are solved by introducing the virtual error parameter. Nevertheless, convergence time of [39] depends on the initial conditions, which might not meet some applications
The newly proposed fixed-time controller has an advantage over the finite-time tracking control where it can guarantee a higher tracking precision. Moreover, the newly proposed controller is more excellent than finite-time results and the settling time of the newly proposed controller which is independent of initial conditions can be designed in advance by modifying parameters.

The rest of this article is organized as follows. Section 2 gives the system description and basic assumption. In Sect. 3, the novel adaptive fixed-time scheme is proposed. Section 4 provides a simulation example to show the effectiveness of the designed scheme. Finally, Sect. 5 contains conclusions and prospects for the future.

2 Problem statement

2.1 Basic assumption and system description

An uncertain nonlinear system with actuator faults in this paper is considered as the following form:

\[
\begin{align*}
\dot{x}_j &= x_{j+1} + f_j (\bar{x}_j), \quad 1 \leq j \leq m - 1 \\
\dot{x}_m &= u^F + \tilde{f}_m (\bar{x}_m) \\
y &= x_1
\end{align*}
\]

where \(\bar{x}_j = [x_1, \ldots, x_j]^T \in \mathbb{R}^j\) denote the system states; \(u^F\) is the input of the system; \(y\) is the output of the system; \(f_j (\bar{x}_j)\) denotes an smooth unknown nonlinear function; for such an uncertain nonlinear system, \(u_k\) is designed when the system is normal. However, in the actual system, there exist failures in the actuators. The following actuator fault model borrowed from [40] and [41] is adopted in this paper

\[
u^F = b (t, t_b) u_k + u_\sigma (t, t_\sigma)
\]

in which the actuator fault \(b (t, t_b) \in [0, 1]\) under consideration is the uncertain time-varying fault; \(u_k\) represents the adaptive controller which lets the closed-loop system be still stable in the event of actuator fault, \(u_\sigma (t, t_\sigma)\) is an additive bias fault; \(t_b\) indicates the point at which the actuator loses its effectiveness; and \(t_\sigma\) represents the time from the normal state to the first additional failure.

Assumption 1 [39] \(b (t, t_b)\) is an unknown time-varying efficiency factor, and \(b_{\min}\) and \(b_{\max}\) represent the known lower and upper bound of \(b (t, t_b)\), respectively. \(u_\sigma (t, t_\sigma)\) is an parameterizable time-varying and bounded function, and it has a upper bound \(u_{\max}\) such that \(|u_\sigma (t, t_\sigma)| \leq u_{\max} (u_{\max} > 0)\).

Remark 1 In (2), if \(b (t, t_b) = 1\) and \(u_\sigma (t, t_\sigma) = 0\), it implies the actuator is normal. If \(b (t, t_b) \neq 1\) and \(u_\sigma (t, t_\sigma) = 0\), it indicates that the actuator is in the presence of loss of effectiveness. In addition, other types of sensor faults may occur at \(b (t, t_b) = 0\) and \(u_\sigma (t, t_\sigma) \neq 0\). As is indicated in Assumption 1, we consider the slow-varying fault whose range of variation is not over 1. It is also worth noting that the additive fault \(u_\sigma (t, t_\sigma)\) cannot be arbitrarily large and is bounded at least by the physical limitation of actuators. In the meantime, \(b (t, t_b)\) and \(u_\sigma (t, t_\sigma)\) are considered unknown, which means that the traditional fixed-time stability criterion is not available. Meanwhile, the
occurrence time is unpredictable for time-varying actuator faults, which may deteriorate system performances and bring certain difficulties to FTC design.

Remark 2 It is noted that there exist no any constraints on the nonlinear term \( f_i (\tilde{x}_i) \) in this paper, which means that the traditional boundary conditions are not required for the considered nonlinearity. Hence, more generalized nonlinear systems are considered in this work.

Definition 1 [42] Give a nonlinear system described by
\[
\dot{x} (t) = g(x(t)), t > t_0
\]
in which \( g(\cdot) \) is continuous, \( x(0) = x_0 \), and \( x \in R^n \) is the state vector. If (3) is globally asymptotically stable with all solutions \( x(t, x_0) \) of (3) converging in finite time by constructing the Lyapunov function, for \( t \geq T_\Phi \), there is finite convergence time \( T_\Phi (x_0) \) that satisfies \( T \leq T_\Phi (x_0) \). Thus, the origin of (3) is globally finite-time stable.

Definition 2 [42] In convergence time, if there is a certain settling time that satisfies \( T \leq T_\Phi \) and system (3) is globally finite-time stable, system (3) is fixed-time stable (FTS).

Lemma 1 [36] Consider system (3), for some scalars \( \varrho_1 > 0, \varrho_2 > 0, 0 < p < 1, q > 0 \) and \( 0 < \sigma < 1 \) and if there exists a positive smooth function \( V(x) \) such that
\[
\dot{V}(x) \leq -\varrho_1 V^p(x) - \varrho_2 V^q(x) + \nu
\]
then the origin of (3) is FTS. Furthermore, for any solution of (3), if there exists the residual set: \( \lim_{t \to T_\Phi} x \mid V(x) \) satisfying the following:
\[
\left\{ \lim_{t \to T_\Phi} x \mid V(x) \leq \min \left\{ \varrho_1^{-\frac{p}{q}} \left( \frac{\nu}{1 - \sigma} \right)^{\frac{1}{q}}, \varrho_2^{-\frac{1}{q}} \right\} \right\}.
\]
The settling time function \( T_\Phi \) can be estimated by
\[
T_\Phi \leq \frac{1 - \varrho_1}{\varrho_1 \sigma \left( 1 - p \right)} + \frac{1}{\varrho_2 \sigma (q - 1)}.
\]
Remark 3 The settling time is bounded by a priori value in fixed-time stability, which is not dependent on initial condition but relying on the control parameters: \( p, q, \varrho_1, \varrho_2 \) and \( \sigma \), which is the biggest difference from finite-time stability. Therefore, the convergence time can be preset in advance under the unknown initial value condition.

Lemma 2 [43] For any given positive constants \( r_1, r_2 \) and \( r_3 \), it holds that
\[
| x | ^p | y | ^q \leq \frac{r_1}{r_1 + r_2} | x | ^r_1 + r_2
\]
\[
+ \frac{r_2}{r_1 + r_3} | y | ^r_3
\]
where \( x \) and \( y \) are any real variables.

Lemma 3 [44] If there exist \( \xi > 0, \forall z \in R \), one can get
\[
0 \leq | z | < \frac{z^2}{\sqrt{z^2 + \xi^2}}.
\]

Lemma 4 [45] If \( l \in [0, 1] \) and there exist some real values \( \xi_1, \ldots, \xi_n \), the following inequality holds
\[
| \xi_1 + \xi_2 + \cdots + \xi_n | \leq | \xi_1 | + \cdots + | \xi_n |.
\]

Lemma 5 [45] For \( \sigma_j \geq 0, j = 1, \ldots, m \), it holds that
\[
(\sigma_1 + \sigma_2 + \cdots + \sigma_m) \leq (\sigma_1^2 + \sigma_2^2 + \cdots + \sigma_m^2).
\]

2.2 Radial basis function neural networks

System (1) contains an unknown nonlinear term, and conventional backstepping method cannot satisfy the design of the controller. In this work, RBFNNs are adopted to approximate the nonlinear function. For example, on a compact set \( \Omega \in R^n \), \( \Theta (Z) \) is a continuous function; \( \xi^T \Phi (Z) \) satisfies the following equality \( \Theta (Z) = \xi^T \Phi (Z) + \zeta (Z) \) in which the ideal weight vector \( \tilde{\xi} = [\xi_1, \xi_2, \ldots, \xi_l] \in R^l \); the approximation error \( \zeta (Z) \) satisfies \( | \zeta (Z) | \leq \pi, \pi > 0 \); \( \Phi (Z) = [\Phi_1 (Z), \ldots, \Phi_l (Z)]^T \) denotes the unit function vector, which composes a Gaussian function; \( l \) is the number of RBFNNs nodes. In this paper, the basic unit of Gaussian function is selected as
\[
\Phi_j (Z) = \exp \left\{ -\frac{\| z - v_j \|^2}{\eta_j} \right\}
\]
where \( v_j = [v_{j1}, v_{j2}, \ldots, v_{jl}] \), \( j = 1, 2, \ldots, l \) is the center in Gaussian function and \( \eta_j \) is the width in Gaussian function. Weight vector \( \xi^*_j \) has the following form
\[
\xi^*_j = \arg \min_{\xi_j \in R^l} \left\{ \sup_{x \in \Omega} \left| \Theta_j (\tilde{Z}_j) - \xi^T_j \Phi_j (Z_j) \right| \right\}
\]
where \( \xi^*_j = \tilde{\xi}_j + \xi_j^* \). Before the controller design, the following assumption is given.
Assumption 2 There exists a sufficiently large compact set $\Omega$ but not infinity, which can cover the system operation field.

Remark 4 In the practical application, the value of the state variable cannot be infinite, and we also have strict requirements for the approximation of nonlinear functions, which cannot be certainly approximated on the basis of infinity. Therefore, it is necessary for Assumption 2 to set up, and all subsequent work will be discussed based on this domain $\Omega$.

3 Controller design and stability analysis

3.1 Fixed-time controller design

First, a signal $y_d$ is introduced, whose $n$th derivative is bounded, available and smooth. Then, combining the backstepping method with the adaptive method, a new scheme will be proposed. The classic form of backstepping is as follows:

$$
\dot{z}_1 = y - y_d \tag{14}
$$

$$
\dot{z}_j = x_j - \varphi_{j-1}(\bar{z}_{j-1}), \ j = 2, \ldots, m \tag{15}
$$

where $\varphi_j(\bar{z}_j)$ is a virtual control law to be designed and $\bar{z}_j$ denotes $[z_1, z_2, \ldots, z_j]$. By using the backstepping approach, one can generate a total control law that forces subsystems to follow the required trajectory for each segment. The details are described as follows:

Step 1: Taking the time derivative of $z_1$ with consideration of system (1), then we get the following results:

$$
\dot{z}_1 = x_2 + f_1(x_1) - \dot{y}_d = z_2 + \varphi_1 + f_1(x_1) - \dot{y}_d. \tag{16}
$$

A Lyapunov function is constructed as follows:

$$
V_1 = \frac{1}{2}z_1^2 + \frac{1}{2b_1}\dot{\theta}_1^2 \tag{17}
$$

where $\dot{\theta}_1 = \theta_1 - \hat{\theta}_1$ is the estimation error in which $\hat{\theta}_1$ is the estimation of $\theta_1$. One has

$$
\dot{V}_1 = z_1(z_2 + \varphi_1 + f_1(x_1) - \dot{y}_d) - \frac{1}{b_1}\dot{\theta}_1 \dot{\theta}_1
= z_1(z_2 + \varphi_1 + \Theta_1(Z_1)) - \frac{1}{b_1}\dot{\theta}_1 \dot{\theta}_1 - \frac{z_1^2}{2}. \tag{18}
$$

The nonlinear function $\Theta_1(Z_1) = f_1(x_1) + z_1/2 - \dot{y}_d$ cannot be available directly due to $\Theta_1(Z_1)$ being related to $f_1(x_1)$, and according to RBFNNs, for $\forall \pi_1 > 0$, $\Theta_1(Z_1)$ is able to be approximated as

$$
\Theta_1(Z_1) = \xi^T_1 \Phi_1(Z_1) + \varsigma_1(Z_1), |\varsigma_1(Z_1)| \leq \pi_1. \tag{19}
$$

Through using simple inequality scaling, one can get

$$
z_1\Theta_1 = z_1 \left(\xi^T_1 \Phi_1 + \varsigma_1\right)
\leq \frac{1}{2a_1^2}z_1^2 \|\xi_1\|^2 \Phi_1^T \Phi_1 + \frac{a_1^2}{2} + \frac{z_1^2}{2} + \frac{\pi_1^2}{2}
\leq \frac{1}{2a_1^2}z_1^2 \theta_1 \Phi_1^T \Phi_1 + \frac{a_1^2}{2} + \frac{z_1^2}{2} + \frac{\pi_1^2}{2} \tag{20}
$$

where $\theta_1 = \|\xi_1\|^2$ and $\Theta_1(Z_1)$ and $\Phi_1(Z_1)$ are abbreviated to $\Theta_1$ and $\Phi_1$, respectively. Substituting (20) into (18) yields that

$$
\dot{V}_1 \leq z_1 z_2 + z_1 \varphi_1 + \frac{1}{2a_1^2}z_1^2 \theta_1 \Phi_1^T \Phi_1 + \frac{a_1^2}{2} + \frac{\pi_1^2}{2}
- \frac{1}{b_1}\dot{\theta}_1 \dot{\theta}_1. \tag{21}
$$

In order to make the subsystem stable, virtual controller is designed as

$$
\varphi_1 = -\frac{z_1^2 \bar{\varphi}_1^2}{\sqrt{z_1^2 \bar{\varphi}_1^2 + z_1^2}}. \tag{22}
$$

By using Lemma 3, the term $z_1 \varphi_1$ in (21) can be expressed as

$$
z_1 \varphi_1 = -\frac{z_1^2 \bar{\varphi}_1^2}{\sqrt{z_1^2 \bar{\varphi}_1^2 + z_1^2}} \leq \zeta_1 - z_1 \bar{\varphi}_1 \tag{23}
$$

where $\bar{\varphi}_1$ can be expressed as

$$
\bar{\varphi}_1 = c_{1.1} \left(\frac{1}{2}\right)^p z_1^{2p-1} + c_{1.2} \left(\frac{1}{2}\right)^q z_1^{2q-1}
+ \frac{1}{2a_1^2}z_1 \hat{\theta}_1 \Phi_1^T \Phi_1 \tag{24}
$$

and the adaptive law is

$$
\dot{\hat{\theta}}_1 = \frac{b_1}{2a_1^2}z_1^2 \Phi_1^T \Phi_1 - \bar{\psi}_1 \hat{\theta}_1 - \frac{c_{1.1}}{b_1} \hat{\theta}_1^3 \tag{25}
$$

where $\zeta_1, c_{1.1}, c_{1.2}, c_1, a_1$ and $b_1$ are all positive constants. Substituting (22)–(25) into (21), one can get

$$
\dot{V}_1 \leq -c_{1.1} \left(\frac{1}{2}\right)^p z_1^{2p} - c_{1.2} \left(\frac{1}{2}\right)^q z_1^{2q} + \zeta_1 z_2 + \Delta_1
+ \bar{\varphi}_1 \hat{\theta}_1 \hat{\theta}_1 + \frac{c_{1.1}}{b_1} \hat{\theta}_1^3 \tag{26}
$$

$$
\hat{\theta}_1 \geq \zeta_1 + z_1 \bar{\varphi}_1 \tag{27}
$$

$$
\dot{V}_1 \geq -c_{1.1} \left(\frac{1}{2}\right)^p z_1^{2p} - c_{1.2} \left(\frac{1}{2}\right)^q z_1^{2q} + \zeta_1 z_2 + \Delta_1
+ \bar{\varphi}_1 \hat{\theta}_1 \hat{\theta}_1 + \frac{c_{1.1}}{b_1} \hat{\theta}_1^3 \tag{28}
$$

$$
\hat{\theta}_1 \geq \zeta_1 + z_1 \bar{\varphi}_1 \tag{29}
$$
\[
\leq -c_{1,1} \left( \frac{z_j^2}{2} \right)^p - c_{1,2} \left( \frac{z_j^2}{2} \right)^q + z_1 z_2 + \Delta_1
\]
\[+ \frac{\ddot{\psi}_i}{b_i} \dot{\phi}_i \dot{\phi}_i + \frac{c_i \ddot{\phi}_i}{b_i} \dot{\phi}_i^3 \]  
(26)

where \( \Delta_1 = (a^2 + \pi_j^2 + 2z_1)/2 \).

Step 1: For \( j = 2, \ldots, m - 1 \): Due to \( z_j = x_j - \phi_j \), where \( \phi_j \) is a virtual control law, one obtains
\[
\dot{z}_j = \dot{x}_j - \dot{\phi}_j - \phi_j = z_{j+1} + \phi_j (\ddot{x}_j) + f_j (\ddot{x}_j) - \dot{\phi}_j - \dot{\phi}_j - \phi_j. \]  
(27)

Consider the Lyapunov function
\[
V_j = \frac{1}{2} z_j^2 + \frac{1}{b_j^2} \dot{\phi}^2_j + V_{j-1}. \]  
(28)

The differential form of \( V_j \) is
\[
\dot{V}_j \leq - \sum_{i=1}^{j-1} c_{i,1} \left( \frac{z_i^2}{2} \right)^p - \sum_{i=1}^{j-1} c_{i,2} \left( \frac{z_i^2}{2} \right)^q
\]
\[+ \sum_{i=1}^{j-1} \frac{\ddot{\psi}_i}{b_i} \dot{\phi}_i \dot{\phi}_i + \sum_{i=1}^{j-1} \frac{c_i \ddot{\phi}_i}{b_i} \dot{\phi}_i^3
\]
\[+ \Delta_{j-1} + z_j \phi_j + z_j \Theta_j - \frac{z_j^2}{2} - \frac{1}{b_j} \dot{\phi}_j \dot{\phi}_i \]  
(29)

where \( \Theta_j = f_j - \phi_j - z_j \phi_j - z_j \phi_j \) denotes a function involved nonlinearity. Similarly, \( \Theta_j \) can be described by
\[
\Theta_j = \xi_j^T \Phi_j + \zeta_j, | \zeta_j | \leq \pi_j. \]  
(30)

Through using simple inequality scaling, one can get
\[
z_j \Theta_j \leq \frac{1}{2a_j^2} z_j^2 \dot{\phi}_j \Phi_j^T \Phi_j + \frac{2}{2} + \frac{\pi_j^2}{2} \]  
(31)

where \( \Theta_j = \| \xi_j \| ^2 \). With the assistance of (23) and Lemma 3, one can get the following result
\[
z_j \phi_j = \frac{z_j^2 \ddot{\phi}_j^2}{\sqrt{z_j^2 \dot{\phi}_j^2 + \zeta_j^2}} \leq \xi_j \phi_j \]  
(32)

\[
\ddot{\phi}_j = c_{j,1} \left( \frac{1}{2} \right)^p z_j^{2p-1} + c_{j,2} \left( \frac{1}{2} \right)^q z_j^{2q-1}
\]
\[+ \frac{1}{2a_j^2} z_j^2 \ddot{\phi}_j \Phi_j^T \Phi_j. \]  
(33)

Accordingly, substituting (31) and (32) into (29), one can get the following inequalities:
\[
\dot{V}_j \leq - \sum_{i=1}^{j-1} c_{i,1} \left( \frac{z_i^2}{2} \right)^p - \sum_{i=1}^{j-1} c_{i,2} \left( \frac{z_i^2}{2} \right)^q
\]
\[+ \sum_{i=1}^{j-1} \frac{\ddot{\psi}_i}{b_i} \dot{\phi}_i \dot{\phi}_i + \sum_{i=1}^{j-1} \frac{c_i \ddot{\phi}_i}{b_i} \dot{\phi}_i^3
\]
\[+ \Delta_{j-1} - \phi_j - \phi_j - \phi_j + \frac{\dot{\phi}_j \dot{\phi}_i}{b_j} \]  
(34)

Similar to the form of (25), it yields
\[
\ddot{\phi}_j = b_j \Phi_j^T \Phi_j - \dot{\phi}_j \dot{\phi}_j - c_j \dot{\phi}_j. \]  
(35)

Furthermore, it follows that
\[
\dot{V}_j \leq - \sum_{i=1}^{j} c_{i,1} \left( \frac{z_i^2}{2} \right)^p - \sum_{i=1}^{j} c_{i,2} \left( \frac{z_i^2}{2} \right)^q
\]
\[+ z_j \phi_j + z_j \phi_j - \frac{z_j^2}{2} - \frac{1}{b_j} \dot{\phi}_j \dot{\phi}_j \]  
(36)

where \( \Delta_j = \left( (2x_j + a^2 + \pi_j^2)/2 \right) - \Delta_{j-1} \).

Step 2: According to the result in step 1, the following equality is satisfied
\[
z_m = \dot{x}_m - \phi_m - \phi_m - \phi_m
\]
\[= u^F + \Phi_m - \Phi_m - \Phi_m
\]
(37)

Select Lyapunov function as follows:
\[
V_m = V_{m-1} + \frac{1}{2} z_m^2 + \frac{1}{2b_m^2} \phi_m^2. \]  
(38)

Its derivative is given as
\[
\dot{V}_m \leq - \sum_{i=1}^{m-1} c_{i,1} \left( \frac{z_i^2}{2} \right)^p - \sum_{i=1}^{m-1} c_{i,2} \left( \frac{z_i^2}{2} \right)^q
\]
\[+ \sum_{i=1}^{m-1} \frac{\ddot{\psi}_i}{b_i} \dot{\phi}_i \dot{\phi}_i + \sum_{i=1}^{m-1} \frac{c_i \ddot{\phi}_i}{b_i} \dot{\phi}_i^3
\]
\[+ \Delta_{m-1} + z_m (\Theta_m + b (t, t_b) u_k + u_{t} (t, t_a))
\]
\[+ \frac{1}{b_m} \dot{\phi}_m \phi_m - \frac{z_m^2}{2} \]  
(39)

where \( \Theta_m = \Phi_m^T \Phi_m + \zeta_m, | \zeta_m | \leq \pi_m \). Similarly, the nonlinear term \( \Theta_m \) can be expressed as
\[
\Theta_m = \xi_m^T \Phi_m + \zeta_m, | \zeta_m | \leq \pi_m \]  
(40)

and it is not difficult to arrive at
\[
z_m \Theta_m \leq \frac{1}{2a_m} z_m^2 \Theta_m \Phi_m^T \Phi_m + \frac{a_m^2}{2} + \frac{z_m^2}{2} + \frac{\pi_m^2}{2} \]  
(41)
where $\theta_m = \| \xi_m \|^2$. Accordingly, combining (35), (41) with (39), it is true that
\[
\dot{V}_m \leq - \sum_{i=1}^{m-1} \sum_{j=1}^q c_{i,1} \left( \frac{z_i^2}{2} \right)^p - \sum_{i=1}^{m-1} \sum_{j=1}^q c_{i,2} \left( \frac{z_i^2}{2} \right)^q \\
+ \sum_{i=1}^{m-1} \sum_{j=1}^q \frac{\tilde{y}_i}{b_i} \tilde{\theta}_i \tilde{\theta}_i \\
+ \sum_{i=1}^{m-1} \sum_{j=1}^q \frac{c_{i,1}}{b_i^2} \tilde{\theta}_i \tilde{\theta}_i^3 \\
+ \Delta_m - 1 + \frac{1}{2a_m^2} z_m \dot{\theta}_m T_m + \frac{a_m^2 + z_m + \pi_m^2}{2} \\
+ z_m b \left( t, t_b \right) u_k + z_m u_\sigma \left( t, t_\sigma \right) \\
- \frac{\tilde{\theta}_m}{2a_m^2} z_m \dot{\theta}_m T_m + \frac{\tilde{\psi}_m}{b_m} \tilde{\theta}_m \tilde{\theta}_m + \frac{c_m}{b_m^2} \tilde{\theta}_m \tilde{\theta}_m^3 \\
- z_m. \quad (42)
\]

With the same manipulation as in (32), it follows that
\[
u_k = - \frac{z_m \tilde{\psi}_m}{b_m \sqrt{z_m \tilde{\psi}_m^2 + \tilde{\zeta}_m^2}} \quad (43)
\]
\[
z_m b \left( t, t_b \right) u_k = - \frac{b \left( t, t_b \right) z_m^2 \tilde{\psi}_m}{b_m \sqrt{z_m \tilde{\psi}_m^2 + \tilde{\zeta}_m^2}} \\
\leq - \frac{z_m \tilde{\psi}_m}{\sqrt{z_m \tilde{\psi}_m^2 + \tilde{\zeta}_m^2}} \leq \zeta_m - z_m \tilde{\psi}_m. \quad (44)
\]

Then, by applying Young’s inequality [46] to terms $z_m u_\sigma \left( t, t_\sigma \right)$, we get
\[
z_m u_\sigma \left( t, t_\sigma \right) \leq \frac{1}{2} \left( z_m^2 + u_\sigma^2 \right). \quad (45)
\]

From (42), (44) and (45), it produces
\[
\dot{V}_m \leq - \sum_{i=1}^m c_{i,1} \left( \frac{z_i^2}{2} \right)^p - \sum_{i=1}^m c_{i,2} \left( \frac{z_i^2}{2} \right)^q \\
+ \sum_{i=1}^m \frac{\tilde{y}_i}{b_i} \tilde{\theta}_i \tilde{\theta}_i \\
+ \sum_{i=1}^m \frac{c_{i,1}}{b_i^2} \tilde{\theta}_i \tilde{\theta}_i^3 \\
+ \frac{a_m^2 + \pi_m^2 + 2 \zeta_m + u_\sigma^2}{2} + \Delta_m - 1 \\
\leq - \sum_{i=1}^m c_{i,1} \left( \frac{z_i^2}{2} \right)^p - \sum_{i=1}^m c_{i,2} \left( \frac{z_i^2}{2} \right)^q \\
+ \sum_{i=1}^m \frac{\tilde{y}_i}{b_i} \tilde{\theta}_i \tilde{\theta}_i \\
+ \sum_{i=1}^m \frac{c_{i,2}}{b_i^2} \tilde{\theta}_i \tilde{\theta}_i^3 + \Delta_m \quad (46)
\]

where $\Delta_m = \left( a_m^2 + \pi_m^2 + 2 \zeta_m + u_\sigma^2 \right) / 2 + \Delta_m - 1$. The proof of the controller design is completed.

3.2 Stability analysis

**Theorem 1** For an uncertain system with actuator faults (1), the controller (43), the parameter adaptive law (35) and the virtual controller (33) are adopted where all the parameters are positive constants, which ensures the tracking errors are convergent in the fixed time with $T$ satisfying $T_\Phi \leq \frac{4}{\varpi_1 \sigma} + \frac{1}{\varpi_2 \sigma}$, the closed-loop system (1) is FTS. Thereinto, all the signals are bounded.

**Proof** This proof is divided into two parts. From Remark 6, the first part displays the boundedness of all variables in the closed-loop system and the second part shows that the output tracks the desired signal $y_d$ to a small neighborhood in fixed time. Detailed proof is given in “Appendix.” \[\square\]

**Remark 5** In the view of the proposed updating law $\tilde{\phi}_j = c_{j,1} \left( \frac{1}{2} \right)^p \tilde{z}_j \tilde{z}_j^{p-1} + c_{j,2} \left( \frac{1}{2} \right)^q \tilde{z}_j \tilde{z}_j^{q-1} + \frac{1}{2a_m^2} \tilde{z}_j \tilde{z}_j \tilde{\phi}_j T \tilde{\phi}_j$, the first term as well as the second term is used to prevent the adaptive parameter growing unboundedly and to ensure its fixed-time convergence, and the third term is used to eliminate neural network approximation error term in stability analysis.

**Remark 6** To some extent, many design parameters determine the control performance. It is noted that the size of parameters $c, \theta, p$ and $q$ can tune convergence error and convergence accuracy simultaneously. Increasing $c_{j,1}, c_{j,2}$ and reducing $\tilde{\phi}_j$ will improve convergence rate and reduce the ultimate error $| y - y_d |$. However, the larger $\tilde{\phi}_j$ is, the poorer updating transient the system has. Similarly, the larger $c_{j,1}, c_{j,2}$ is,
Fig. 3  Trajectory of tracking error $y - y_d$

Fig. 4  Trajectories of $y$ and $y_d$

Fig. 5  Trajectories of $u_k$ and $u^F$

Fig. 6  Trajectories of $\hat{\theta}_1$ and $\hat{\theta}_2$ under $u_\sigma (t, t_\sigma) = \cos^2 (x_2)$

the higher control input is. $|y - y_d|$ is related to $\zeta_j$. Concretely, smaller $\zeta_j$ will reduce ultimate error. From Lemma 3, $\zeta_j$ cannot be zero. The neural network approximation error will be reduced because of large neurons number $l$ resulting in affecting $\varphi_j$ and further affecting error. Thus, $|y - y_d|$ only enters into the range near the origin in fixed time due to the system functions and actuator failures being unknown.

4 Simulation results

This section provides a numerical example to show the effectiveness of our control strategy. Consider a second-order system described as: follows:

$$
\begin{align*}
\dot{x}_1 &= x_2 + f_1 (x_1) \\
\dot{x}_2 &= u^F + f_2 (x_1, x_2) \\
y &= x_1
\end{align*}
$$

(47)

where $f_1 (x_1) = \sin (x_1) + (x_1^2) / (1 + x_1^2)$, $f_2 (x_1, x_2) = x_1 x_2$. An additional actuator fault $u_\sigma (t, t_\sigma) = x_2 \cos^2 (x_1)$ is set up. In addition, the time-varying coefficient is chosen as $b (t, t_\sigma) = 0.4 + 0.6 \exp (-0.2t)$. First of all, assuming that the reference signal is $y_d = 0.8 \sin t \cos 0.5t$. That the output signal can track the desired signal $y_d$ is the target of the controller. According to Theorem 1, $\tilde{\varphi}_1$, $\tilde{\varphi}_2$ and the adaptive law of $\hat{\theta}_i$ are as follows

$$
\tilde{\varphi}_1 = c_{1.1} \left( \frac{1}{2} \right)^{\frac{3}{2}} z_1^{\frac{1}{2}} + c_{1.2} \left( \frac{1}{2} \right)^{\frac{2}{3}} z_1^{\frac{1}{2}}
$$
Adaptive fixed-time control for nonlinear systems

A fixed-time control issue for nonlinear systems with unknown actuator failures has been addressed in this paper. A new fixed-time adaptive neural networks control scheme has been designed to cope with this problem where the unknown actuator failures are considered and the uncertain nonlinearities of the system is unknown. Compared with the existing results, the new control scheme becomes more applicable in practice. In addition, a newly adaptive fixed-time controller can estimate actuator faults, which can guarantee that the system is FTS. Meanwhile, all signals are bounded in the closed-loop system and the approximation of uncertain nonlinear functions is proved to be feasible. The proposed control method does not require initial conditions of the considered systems and can successfully compensate for actuator faults. Simulation results have shown that the scheme in this paper can provide faster convergence speed than finite-time control. In addition, disturbance and parameterization problems are not considered in this paper, which are worth studying. For future study, we will be devoted to dealing with more complicated nonlinear functions with the help of neural network systems, which will get more conclusions about fixed-time control.

5 Conclusion

A fixed-time control issue for nonlinear systems with unknown actuator failures has been addressed in this paper. A new fixed-time adaptive neural networks control scheme has been designed to cope with this problem where the unknown actuator failures are considered and the uncertain nonlinearities of the system is unknown. Compared with the existing results, the new control scheme becomes more applicable in practice. In addition, a newly adaptive fixed-time controller can estimate actuator faults, which can guarantee that the system is FTS. Meanwhile, all signals are bounded in the closed-loop system and the approximation of uncertain nonlinear functions is proved to be feasible. The proposed control method does not require initial conditions of the considered systems and can successfully compensate for actuator faults. Simulation results have shown that the scheme in this paper can provide faster convergence speed than finite-time control. In addition, disturbance and parameterization problems are not considered in this paper, which are worth studying. For future study, we will be devoted to dealing with more complicated nonlinear functions with the help of neural network systems, which will get more conclusions about fixed-time control.

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Conflict of interest The authors declare that they have no conflict of interest.

Appendix

Consider the Lyapunov function as follows:

\[ V_m = \frac{1}{2} z_m^2 + \frac{1}{2 m} \tilde{\theta}_m^2. \]  

(49)

According to the definition of \( \tilde{\theta}_i \), one can get the following inequality:

\[ \tilde{\theta}_i \tilde{\theta}_i = \tilde{\theta}_i \left( \theta_i - \hat{\theta}_i \right) \leq -\frac{1}{2} \tilde{\theta}_i^2 + \frac{1}{2} \theta_i^2 \]  

(50)

and motivated by the literature [46], just to facilitate the description of the binomial theorem \( (\theta_i - \tilde{\theta}_i)^3 \), \( p = 3/4 \) and \( q = 2 \) are used to demonstrate stability. Based on (49), (50), Lemmas 5 and 6, then the time derivative of \( V_m \) is

\[ \dot{V}_m \leq \sum_{i=1}^{m} \frac{\tilde{\psi}_i \tilde{\theta}_i \tilde{\theta}_i}{b_i} + \sum_{i=1}^{m} \frac{c_i \tilde{\theta}_i \tilde{\theta}_i^3}{b_i^2} - \sum_{i=1}^{m} c_{i,1} \left( \frac{z_i^2}{2} \right)^{3/4} \]  

\[ \leq -\tilde{\theta}_1 \left( \sum_{i=1}^{m} \frac{z_i^2}{2} \right) - \tilde{\theta}_2 \left( \sum_{i=1}^{m} \frac{z_i^2}{2} \right)^{3/4} + \Delta_m \]  

(51)

where \( \tilde{\theta}_1 = \min \left( c_{i,1}, \ldots, c_{m,1}, \tilde{\psi}_1, \ldots, \tilde{\psi}_m \right) \), \( \tilde{\theta}_2 = \min \left( c_{i,1}, \ldots, c_{m,1} \right) \).

Applying Lemma 2 to the term \( \frac{\tilde{\psi}_i \tilde{\theta}_i^2}{2 b_i} \), we can obtain that

\[ \left( \frac{\tilde{\psi}_i \tilde{\theta}_i^2}{2 b_i} \right)^{\gamma} \leq (1 - \gamma) \gamma^{\gamma \theta} + \frac{\tilde{\psi}_i \tilde{\theta}_i^2}{2 b_i}. \]  

(52)

Combining (52) and (51), one has

\[ \dot{V}_m \leq -\tilde{\theta}_1 \left( \sum_{i=1}^{m} \frac{z_i^2}{2} \right)^{3/4} - \tilde{\theta}_2 \left( \sum_{i=1}^{m} \frac{z_i^2}{2} \right)^{3/4} + \tilde{\theta}_1 \sum_{i=1}^{m} \frac{\tilde{\psi}_i \tilde{\theta}_i^2}{2 b_i} + \tilde{\theta}_2 \sum_{i=1}^{m} \frac{c_i \tilde{\theta}_i \tilde{\theta}_i^3}{b_i^2} + \tilde{\theta}_1 \sum_{i=1}^{m} \frac{c_i \tilde{\theta}_i \tilde{\theta}_i^3}{b_i^2} + \Delta_m. \]  

(53)

Combining (55), (56) with (54) yields

\[ \dot{V}_m \leq -\tilde{\theta}_1 \left( \sum_{i=1}^{m} \frac{z_i^2}{2} \right)^{3/4} - \tilde{\theta}_2 \left( \sum_{i=1}^{m} \frac{z_i^2}{2} \right)^{3/4} + \tilde{\theta}_1 \sum_{i=1}^{m} \frac{\tilde{\psi}_i \tilde{\theta}_i^2}{2 b_i} + \tilde{\theta}_2 \sum_{i=1}^{m} \frac{c_i \tilde{\theta}_i \tilde{\theta}_i^3}{b_i^2} + \Delta_m. \]  

(57)
where \( v = \dot{\nu} + \sum_{i=1}^{m} \frac{3c_i \nu_i^4}{4 \lambda_i b_i} + \sum_{i=1}^{m} \frac{c_i \nu_i^6}{12 \lambda_i b_i} \). Moreover, equation (57) can be rewritten as:

\[
\dot{V}_m \leq -\tilde{q}_1 \left( \sum_{i=1}^{m} \frac{\nu_i^2}{2} \right)^{\frac{3}{4}} - \tilde{q}_1 \left( \sum_{i=1}^{m} \frac{\nu_i^2}{2} \right)^{\frac{3}{4}}
- \tilde{q}_2 \left( \sum_{i=1}^{m} \frac{\nu_i^2}{2} \right)^{\frac{3}{2}} - \tilde{q}_2 \left( \sum_{i=1}^{m} \frac{\nu_i^2}{2} \right)^{\frac{3}{2}} + v \tag{58}
\]

where \( \tilde{q}_2 = \min \left( \left( 4 - 9 \tilde{q}_1 \right) c_i, \frac{\tilde{v}_m}{m} \right) \); we can get

\[
\dot{V}_m \leq -\tilde{q}_1 \left( \sum_{i=1}^{m} \frac{\nu_i^2}{2} \right)^{\frac{3}{4}} + \left( \sum_{i=1}^{m} \frac{\nu_i^2}{2} \right)^{\frac{3}{4}}
- \tilde{q}_2 \left( \sum_{i=1}^{m} \frac{\nu_i^2}{2} \right)^{\frac{3}{2}} + \left( \sum_{i=1}^{m} \frac{\nu_i^2}{2} \right)^{\frac{3}{2}} + v. \tag{59}
\]

Applying Lemmas 4 and 5 to \( \dot{V}_m \), one can get

\[
\dot{V}_m \leq -\tilde{q}_1 V_m^3 - \tilde{q}_2 V_m^2 + v \tag{60}
\]

where \( \tilde{q}_2 = \tilde{q}_2, \tilde{q}_1 = \tilde{q}_1 \).

At the same time, it follows from (60) that

\[
\dot{V}_m \leq -\tilde{q}_2 V_m^3 - \sigma \tilde{q}_1 V_m^2 - (1 - \sigma) \tilde{q}_1 V_m^2 + v \tag{61}
\]

where \( 0 < \sigma < 1 \). If \( v - (1 - \sigma) \tilde{q}_1 V_m^2 < 0 \), by Lemma 1, one can obtain

\[
T \leq \frac{4}{\tilde{q}_1 \sigma} + \frac{1}{\tilde{q}_2} \tag{62}
\]

It also follows from (60) that

\[
\dot{V}_m \leq -\sigma \tilde{q}_2 V_m^3 - \tilde{q}_1 V_m^2 - (1 - \sigma) \tilde{q}_2 V_m^3 + v \tag{63}
\]

where \( 0 < \sigma < 1 \). If \( v - (1 - \sigma) \tilde{q}_2 V_m^2 < 0 \). By applying Lemma 1, it follows

\[
T \leq \frac{1}{\tilde{q}_2 \sigma} + \frac{4}{\tilde{q}_1}. \tag{64}
\]

By using Lemma 1, that the system is FTS can be obtained and one can get

\[
V(x) = \min \left\{ \tilde{q}_1^{\frac{1}{p}} \left( \frac{\nu}{1 - \sigma} \right)^{\frac{1}{p}}, \tilde{q}_2^{\frac{1}{p}} \left( \frac{\nu}{1 - \sigma} \right)^{\frac{1}{p}} \right\}, \tag{65}
\]

\[
T \Phi \leq \frac{4}{\tilde{q}_1 \sigma} + \frac{1}{\tilde{q}_2 \sigma}. \tag{66}
\]

According to the definition of \( V(x) \), it can be concluded that, for \( \Xi \triangleq (2 \tilde{q}_1^{\frac{1}{p}} \left( \frac{\nu}{1 - \sigma} \right)^{\frac{1}{p}}, | z_j | \leq \Xi \), and \( | y - y_d | \leq \Xi \). In other words, the output can track the desired signal \( y_d \) to a small neighborhood in fixed time.

On the basis of (60), it is not hard to derive that \( V_m < 0 \), when \( V_m^2 \geq v/\tilde{q}_2 \). Obviously, it can be observed that all the state variables \( x_j \) are bounded. This completes the proof.

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