Article

Fast Frame Synchronization Design and FPGA Implementation in SF-BOTDA

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Abstract: To address the issues of high time consumption of frame synchronization involved in a scanning-free Brillouin optical time-domain analysis (SF-BOTDA) system, a fast frame synchronization algorithm based on incremental updating was proposed. In comparison to the standard frame synchronization algorithm, the proposed one significantly reduced the processing time required for the BOTDA system frame synchronization by about 98%. In addition, to further accelerate the real-time performance of frame synchronization, a field programmable gate array (FPGA) hardware implementation architecture based on parallel processing and pipelining mechanisms was also proposed. Compared with the software implementation, it further raised the processing speed by 13.41 times. The proposed approach could lay a foundation for the BOTDA system in the field with the associated high real-time requirements.

Keywords: Brillouin optical time-domain analysis; frame synchronization; field programmable gate array; incremental updating

1. Introduction

In recent decades, distributed Brillouin optical time domain analyzer (BOTDA) has been intensively investigated for a wide variety of applications, including temperature analysis [1,2] and structure health monitoring [3,4]. It’s capability to provide highly precise and distributed measurements of strain and temperature profiles has been demonstrated [5,6]. However, due to the frequency-scanning nature, the acquisition time and post-processing time of most existing BOTDAs can vary from seconds to minutes when sensing ranges and spatial resolutions changes [7–10], which limits its development in the field of fast distributed monitoring systems, such as a vibration measuring system for long sensing range and high spatial resolution for civil or aeronautic structures applications [11,12].

To solve the problem of long acquisition times, a variety of scanning-free BOTDA (SF-BOTDA) or single-shot methods was proposed [13–18]. For example, slope-assisted BOTDA is realized based on tuning the frequency of probe optical signal to half of BGS which can effectively shorten the measurement time [13]. In Ba et al. [14], another kind of scanning-free BOTDA is proposed based on multiple probes and pump pairs that allows for the fast measurement of strain or temperature changes along the fiber. Moreover, Jin et al. proposed a digitally generated optical-frequency-comb-based BOTDA to realize scanning-free BOTDA and single measurement BOTDA in 2015 and 2017 respectively, with an acquisition time of 100 µs for a 10 km optical fiber [15,16]. In Fang et al. [17], a dual-polarization probe with orthogonal frequency-division multiplexing (OFDM) modulation is used for a single-shot BOTDA system where frequency scanning and polarization scrambling are no longer required. A single-shot BOTDA based on an optical chirp chain probe wave is also proposed for distributed
ultrafast measurements with a sampling rate of up to the MHz level [18]. These efforts mean that the time consumption of acquisition is no longer the bottleneck of a real-time BOTDA.

Although SF-BOTDA can significantly reduce the time consumption of acquisition, it produces a huge amount of data and requires complicated calculations in the subsequent data processing, such as frame synchronization, fast Fourier transform (FFT), and phase calculation, which has become a new factor restricting the BOTDA system’s real-time application [15,16]. During post-processing, synchronization is only required to be implemented once such that the SF-BOTDA system can keep running until the fiber sensing data acquisition is completed. However, such a synchronization process usually takes a few milliseconds, and since the subsequent data processing can only be carried out after the completion of frame synchronization, the time consumed by synchronization will affect the real-time performance of the BOTDA system.

To address issues regarding the high time consumption of the frame synchronization present in the SF-BOTDA system, a novel frame synchronization algorithm was proposed. The proposed algorithm can avoid a lot of redundant calculations for frame synchronization by using the incremental updating method, and therefore reduce the computational complexity. In addition, to further accelerate the real-time performance of frame synchronization, a field programmable gate array (FPGA) hardware implementation architecture based on parallel processing and pipelining mechanisms was also proposed.

2. Basic Principle

2.1. Frame Synchronization

The simplified schematic principle of SF-BOTDA system is shown in Figure 1, where after the probe with flat spectrum collides with the pump in the optical fiber, part of the energy of the pump is transferred to the probe due to the Brillouin frequency shift (BFS), converting the flat spectrum into a spectrum with a gain peak. The BFS has a linear relationship with temperature and strain, therefore the detection of temperature or strain can be realized via monitoring the BFS [5,6]. The probe is a periodic frame sequence modulated by an electro-optic modulator (EOM), which interacts with the pump in sequence and records the BFS, which is organized into each of its independent frames. At the receiver end, after the frame synchronization, fast Fourier transform (FFT), and Brillouin gain spectrum (BGS) measurements, the BFS of different positions can be obtained. It can be seen that in the SF-BOTDA system, frame synchronization is the first step of data processing and a guarantee and premise for subsequent data analysis.

Figure 1. Simplified schematic representation of the principle of the scanning-free Brillouin optical time domain analyzer (SF-BOTDA) system.

The problem of locating the frame separation position is called frame synchronization. Furthermore, the synchronization algorithms can be divided into data-aided and non-data-aided methods depending
on whether additional symbols are needed in the process of synchronization. The basic idea of the data-aided method is the use of a training sequence or pilot signal as an auxiliary to realize synchronization based on the self-correlation of the received sequence or the cross-correlation between the received sequence and local reference sequence. The non-data-aided method constructs a new frame structure by using cyclic prefix (CP) or empty subcarriers to realize synchronization, as shown in Figure 2. Since CP is a copy of $N$ sample points of the original frame tail, there is the greatest correlation between them, and the frame separation position can be located correctly by comparing the correlation between sequences of different positions.

![Figure 2. Schematic diagram of frame synchronization method. FUT: fiber under test; CP: cyclic prefix.](image)

In fact, the core idea of synchronization is the same whether a data-aided method or non-data-aided method is adopted, that is, the correlation between sequences of different positions is constantly calculated to find the position with the highest correlation as the result of the synchronization. In this paper, the non-data-aided method with CP will be illustrated as an example.

Mathematically, for a frame with $M$ sample points, $M$ times correlations need to be calculated to locate the frame synchronization position, and the correlation of the sequences is measured using a normalized cross-correlation coefficient (NCC). For sequences $A(i)$ and $B(i)$ in position $i$, the NCC is defined as:

$$C_{NC}(i) = \frac{\sum_{j=1}^{N} (A(i,j) - \bar{A}(i)) (B(i,j) - \bar{B}(i))}{\sqrt{\sum_{j=1}^{N} (A(i,j) - \bar{A}(i))^2 \times \sum_{j=1}^{N} (B(i,j) - \bar{B}(i))^2}}, \quad i \in [1, M],$$

(1)

where $A(i,j)$ and $B(i,j)$ are the $j$-th sample point of sequences $A(i)$ and $B(i)$, respectively, and $\bar{A}(i)$ and $\bar{B}(i)$ are the respective mean values of them, which are defined as:

$$\bar{A}(i) = \frac{\sum_{j=1}^{N} A(i,j)}{N}, \quad i \in [1, M],$$

(2)

$$\bar{B}(i) = \frac{\sum_{j=1}^{N} B(i,j)}{N}, \quad i \in [1, M].$$

(3)

From Equations (1)–(3), the calculation of $C_{NC}(i)$ for two sequences with $N$ samples requires $(3 \times N + 4)$ multiplications and $(7 \times N - 5)$ summations. Furthermore, for the frame shown in Figure 2, $M$ times NCC calculations are required for the location of the frame synchronization position; to process this number of calculations, millions of operations are needed, which can be quite a challenge for a real-time BOTDA system. Hence, it is necessary to find out a way to reduce the calculation complexity of the frame synchronization.

2.2. Fast Frame Synchronization Method

In the process of frame synchronization, since the cached sequence $A(i+1)$ and $B(i+1)$ are only one sample delay from $A(i)$ and $B(i)$, respectively, there is a larger amount of computational redundancy.
between them. Some methods can be taken to avert repeatedly calculating the terms in the nominator and denominator at each calculation step of Equation (1).

Let \( V_{CO}(i) = \sum_{j=1}^{N}[A(i, j) - A(i)] \times [B(i, j) - B(i)] \), \( V_A(i) = \sum_{j=1}^{N}[A(i, j) - A(i)]^2 \), and \( V_B(i) = \sum_{j=1}^{N}[B(i, j) - B(i)]^2 \), such that Equation (1) can be simplified to:

\[
C_{NC}(i) = \frac{V_{CO}(i)}{\sqrt{V_A(i) \times V_B(i)}}, \quad i \in [1, M]. \tag{4}
\]

For \( V_{CO} \), the value of position \((i+1)\) has the following relationship with the value of position \(i\):

\[
V_{CODIF}(i + 1) = V_{CO}(i + 1) - V_{CO}(i)
\]
\[
= \sum_{j=1}^{N}[A(i + 1, j) - A(i + 1)] \times [B(i + 1, j) - B(i + 1)]
- \sum_{j=1}^{N}[A(i, j) - A(i)] \times [B(i, j) - B(i)],
\tag{5}
\]

which can be simplified to:

\[
V_{CODIF}(i + 1) = V_{CO}(i + 1) - V_{CO}(i)
\]
\[
= [A(i + 1, N) - A(i, 1)] \times [B(i + 1, N) - B(i + 1)]
- [B(i, 1) - B(i + 1)] \times [A(i, 1) - A(i)].
\tag{6}
\]

It can be seen that \( V_{CO}(i + 1) \) can be calculated through two multiplications and five summations on the basis of \( V_{CO}(i) \). Compared with the direct calculation method, which requires \( N \) multiplications and \((3 \times N - 1)\) summations, the computational complexity is significantly reduced.

Similarly, one can derive that:

\[
V_{ADIF}(i + 1) = V_A(i + 1) - V_A(i)
\]
\[
= [A(i + 1, N) - A(i, 1)] \times [A(i, 1) + A(i + 1, N) - A(i + 1) - A(i)],
\tag{7}
\]

\[
V_{BDIF}(i + 1) = V_B(i + 1) - V_B(i)
\]
\[
= [B(i + 1, N) - B(i, 1)] \times [B(i, 1) + B(i + 1, N) - B(i + 1) - B(i)].
\tag{8}
\]

Substituting Equations (6)–(8) into Equation (1), one can rewrite the \( M \) times NCC calculations for frame synchronization as:

\[
C_{NC}(i) = \left\{ \frac{\sum_{j=1}^{N}[A(i, j) - A(i)] \times [B(i, j) - B(i)]}{\sqrt{\sum_{j=1}^{N}[A(i, j) - A(i)]^2 \times \sum_{j=1}^{N}[B(i, j) - B(i)]^2} \times \sqrt{V_{ADIF}(i) + V_{CODF}(i - 1) + V_{BDIF}(i - 1) + V_B(i - 1)}}, \quad i \in [2, M] \right. \tag{9}
\]

Therefore, in light of Equation (9), it can be seen that the calculation complexity is substantially reduced to \((3 \times N + 4) + 8 \times (M - 1)\) multiplications and \((7 \times N - 5) + 16 \times (M - 1)\) summations. For the \( M = 1152 \) and \( N = 128 \) used in References [14,15], using the standard method requires 446,976 multiplications and 1,026,432 summations, while using the proposed method only required 9596 multiplications and 19,307 summations, reducing the calculation amount by about 98%, which makes the real-time frame synchronization in BOTDA possible.

2.3. FPGA Implementation

In order to further improve the real-time performance of the BOTDA system, parallel and pipeline mechanisms of FPGA can be used to reduce the time consumption of data processing [19–21]. The hardware architecture of the proposed method implemented on an FPGA is shown in Figure 3, consisting of three parts: (1) data caching module, (2) moving NCC module, and (3) result output.
module. Among them, the data caching module is used for data access control and format conversion, the moving NCC module calculates the M times NCC calculations, and the result output module compares the NCC value of each position to find the frame synchronization position.

![Figure 3. FPGA block diagram of the proposed frame synchronization method.](image)

In the moving NCC module, for the purpose of speeding up the frame synchronization, the NCC parallel structure is proposed, as shown in Figure 4, which consists of two main parts: (1) first NCC and (2) non-first NCC. For the first NCC parts, parallel computation is employed for each calculation step to speed up the real-time frame synchronization. For example, at the step of normalizing the inputted raw data, the parallel subtractor (Psub) that parallelly subtracts the original value of each sequence from their mean that is calculated first with a parallel accumulator (Pacc) and a right-shift operation is implemented. After the Psub, the normalized sequence is ready for the input of a parallel multiply-accumulator (Pmac) to calculate $V_{C(1)}$, $V_{A(1)}$, and $V_{B(1)}$, respectively. Then, the final result of $C_{NC}(1)$ can be obtained by using Equation (9). For the non-first NCC calculation, it is much easier than the first NCC since it just requires the calculation of the values of $V_{ADIF(i)}$, $V_{BDIF(i)}$, and $V_{CODEF(i)}$. By reusing the last time results of $V_{CO}$, $V_{A}$, and $V_{B}$, it is easy to obtain the value of the non-first NCC according to Equation (9). The above steps adopt a pipelining mechanism, where under the control of clock (CLK), sequence data can be continuously inputted and the calculation result can be continuously outputted after a certain initial delay.

![Figure 4. NCC parallel processing architecture. Dif: difference, Pacc: parallel accumulator, Pmac: parallel multiply-accumulator, Psub: parallel subtractor.](image)
3. Experimental Results and Analysis

To compare the accuracy of computation between the proposed method and the standard frame synchronization method, random data with different signal to noise ratios (SNRs) with $M = 1152$ and $N = 128$ were input to the system. Under the situations of SNR adjusted from 5 dB to 20 dB changing with 5 dB steps, as shown in Figure 5, the proposed method was consistent with the standard method for calculating the NCC value of the different position in MATLAB (R2017b, 64-bit, MathWorks, NATICK, MA, U.S.), which verified the correctness of the proposed method. Furthermore, it can be seen that the NCC value of different positions had a slight deviation between the platforms of MATLAB and FPGA, which was inevitable because of the finite word-length effect of division and square root operation in FPGA implementation. Furthermore, the zoomed images show that the position of the maximum NCC was the same between different platforms and methods, indicating that both the proposed fast frame synchronization method and the FPGA implementation could locate the frame separation position correctly.

![Figure 5](image_url)

**Figure 5.** NCC deviation between different methods and platforms with different signal to noise ratios (SNRs): (a) SNR = 5 dB, (b) SNR = 10 dB, (c) SNR = 15 dB, and (d) SNR = 20 dB.

The comparison of the running time between the proposed fast frame synchronization method and the standard method on different platforms is shown in Table 1. It can be seen that in the MATLAB platform, compared with the standard method, which needed 9227 $\mu$s for the frame synchronization, the proposed method only took 55 $\mu$s, which reduced the running time by over 99.4%. Further, the FPGA implementation of the proposed method only needed 4.1 $\mu$s to perform the same operation, and the time performance was improved by 13.41 times compared with software implementation, which indicates that the parallel processing and pipeline mechanism could further accelerate the frame synchronization of BOTDA. The experimental result of Table 1 shows that
the proposed method and FPGA implementation could effectively reduce the time consumption required for frame synchronization and lay a foundation for the BOTDA system in the field with high real-time requirements.

**Table 1. Running time of different methods and platforms.**

| Algorithms          | Standard Method (MATLAB) | Standard Method (FPGA) | Proposed Method (MATLAB) | Proposed Method (FPGA) |
|---------------------|--------------------------|------------------------|--------------------------|------------------------|
| Execution Time (µs) | 9227                     | 27                     | 55                       | 4.1                    |

Table 2 shows the influence of the different methods used to complete frame synchronization on the real-time performance of the BOTDA system. In order to realize real-time BOTDA, the parallel and pipeline mechanisms of FPGA were adopted to achieve the rate consistency of data acquisition and data processing. As a result, for the implemented BOTDA system, the processing result of input sensor data could be continuously output after the initial delay. Note that since the subsequent piecewise data processing could only be carried out after the completion of frame synchronization in a pipelined manner, the initial delay consisted of the time consumed by frame synchronization and the data processing of the first frame. As shown in Table 2, the initial delay was mainly limited by the frame synchronization when the standard synchronization method was adopted, and it could be significantly reduced if we used the proposed synchronization method, which meant the real-time performance of the BOTDA system was better.

**Table 2. The effect of different methods on the real-time performance of the BOTDA system.**

|                      | Time of Frame Synchronization ($t_{\text{syn}}$) | Time of Data Processing of First Frame ($t_d$) | Initial Delay ($t_{\text{init}} = t_{\text{syn}} + t_d$) |
|----------------------|-----------------------------------------------|-----------------------------------------------|-------------------------------------------------------|
| Standard Method (FPGA) | 27.0 µs                                       | 6.6 µs                                        | 33.6 µs                                               |
| Proposed Method (FPGA) | 4.1 µs                                        | 6.6 µs                                        | 10.7 µs                                               |

4. Conclusions

To fulfill the real-time requirements of frame synchronization in BOTDA, a novel frame synchronization method based on incremental updating was proposed. Experimental results show that the proposed method could correctly locate the frame separation position and significantly shorten the computing time required for frame synchronization in the BOTDA system. In addition, the parallel and pipeline mechanisms of FPGA were used to further improve the real-time performance of frame synchronization, which can lay a foundation for the real-time application of the BOTDA system.

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**References**

1. Kwon, I.; Kim, C.; Choi, M. Distributed Strain and Temperature Measurement of a Beam Using Fiber Optic Botda Sensor. In *Smart Structures and Materials 2003: Smart Systems and Nondestructive Evaluation for Civil Infrastructures*; International Society for Optics and Photonics: Bellingham, MA, USA, 2003; Volume 5057, pp. 486–496.

2. Li, S.; Zhao, B.; Huang, D. Experimental and numerical investigation on temperature measurement of BOTDA due to drop leakage in soil. *J. Loss Prev. Process Ind.* 2016, 41, 1–7. [CrossRef]
3. Nishio, M.; Mizutani, T.; Takeda, N. Structural shape identification using distributed strain data from PPP-BOTDA. In Sensor Systems and Networks: Phenomena, Technology, and Applications for NDE and Health Monitoring 2007; International Society for Optics and Photonics: San Diego, CA, USA, 2007.

4. Bao, Y.; Hoeher, M.S.; Smith, C.M.; Bundy, M.; Chen, G. Temperature Measurement and Damage Detection in Concrete Beams Exposed to Fire Using PPP-BOTDA Based Fiber Optic Sensors. Smart Mater. Struct. 2017, 26, 105034. [CrossRef] [PubMed]

5. Horiguchi, T.; Tateda, M. Optical-fiber-attenuation investigation using stimulated Brillouin scattering between a pulse and a continuous wave. Opt. Lett. 1989, 14, 408–410. [CrossRef] [PubMed]

6. Kurashima, T.; Horiguchi, T.; Tateda, M. Distributed-Temperature Sensing Using Stimulated Brillouin Scattering in Optical Silica Fibers. Opt. Lett. 1990, 15, 1038–1040. [CrossRef]

7. Dong, Y.; Ba, D.; Jiang, T.; Zhou, D.; Zhang, H.; Zhu, C.; Lu, Z.; Li, H.; Chen, L.; Bao, X. High-Spatial-Resolution Fast BOTDA for Dynamic Strain Measurement Based on Differential Double-Pulse and Second-Order Sideband of Modulation. IEEE Photon. J. 2013, 5, 2600407. [CrossRef]

8. Sovran, I.; Motil, A.; Tur, M. Frequency-Scanning BOTDA With Ultimately Fast Acquisition Speed. IEEE Photon. Technol. Lett. 2015, 27, 1426–1429. [CrossRef]

9. Sperber, T.; Eyal, A.; Tur, M.; Thévenaz, L. High spatial resolution distributed sensing in optical fibers by Brillouin gain-profile tracing. Opt. Express 2010, 18, 8671–8679. [CrossRef] [PubMed]

10. OzOptics, Fiber Optic Distributed Strain and Temperature Sensor (DSTS), DTS0139 Datasheet. Available online: https://www.ozoptics.com/ALLNEW_PDF/DTS0139.pdf (accessed on 3 January 2018).

11. Zheng, H.; GE, H.; Feng, Y. Applications in bridge structure health monitoring using distributed fiber sensing. In AOPC 2017: Fiber Optic Sensing and Optical Communications; International Society for Optics and Photonics: Bellingham, MA, USA, 2017; Volume 10464, p. 104640I.

12. Diakaridia, S.; Pan, Y.; Xu, P.; Zhou, D.; Wang, B.; Teng, L.; Lu, Z.; Ba, D.; Dong, Y. Detecting cm-scale hot spot over 24-km-long single-mode fiber by using differential pulse pair BOTDA based on double-peak spectrum. Opt. Express 2017, 25, 17727–17736. [CrossRef]

13. Peled, Y.; Motil, A.; Yaron, L.; Tur, M. Slope-assisted fast distributed sensing in optical fibers with arbitrary brillouin profile. Opt. Express 2011, 19, 19845–19854. [CrossRef] [PubMed]

14. Ba, D.; Wang, B.; Zhou, D.; Yin, M.; Dong, Y.; Li, H.; Lu, Z.; Fan, Z. Distributed measurement of dynamic strain based on multi-slope assisted fast BOTDA. Opt. Express 2016, 24, 9781. [CrossRef] [PubMed]

15. Jin, C.; Guo, N.; Feng, Y.; Wang, L.; Liang, H.; Li, J.; Li, Z.; Yu, C.; Lu, C. Scanning-free BOTDA based on ultra-fine digital optical frequency comb. Opt. Express 2015, 23, 5277–5284. [CrossRef] [PubMed]

16. Jin, C.; Wang, L.; Chen, Y.; Guo, N.; Chung, W.; Au, H.; Li, Z.; Tam, H.-Y.; Lu, C. Single-measurement digital optical frequency comb based phase-detection Brillouin optical time domain analyzer. Opt. Express 2017, 25, 9213–9224. [CrossRef] [PubMed]

17. Fang, J.; Xu, P.; Dong, Y.; Shieh, W. Single-shot distributed Brillouin optical time domain analyzer. Opt. Express 2017, 25, 15188. [CrossRef]

18. Zhou, D.; Dong, Y.; Wang, B.; Pang, C.; Ba, D.; Zhang, H.; Lu, Z.; Li, H.; Bao, X. Single-shot BOTDA based on an optical chirp chain probe wave for distributed ultrafast measurement. Light Sci. Appl. 2018, 7, 32. [CrossRef] [PubMed]

19. Abbasnejad, M.; Alizadeh, B. FPGA-Based Implementation of a Novel Method for Estimating the Brillouin Frequency Shift in BOTDA and BOTDR Sensors. IEEE Sens. J. 2017, 18, 2015–2022. [CrossRef]

20. Wu, H.; Wang, H.; Choy, C.-S.; Lu, C. BOTDA Fiber Sensor System Based on FPGA Accelerated Support Vector Regression. arXiv 2018, arXiv:preprint 1901.01141. [CrossRef]

21. Abbasnezhad, M.; Alizadeh, B. FPGA-Based Implementation of an Artificial Neural Network for Measurement Acceleration in BOTDA Sensors. IEEE Trans. Instrum. Meas. 2018, 68, 4326–4334. [CrossRef]

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