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Evaluating the use of machine learning in the assessment of joint angle using a single inertial sensor

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Abstract

Introduction: Joint angle measurement is an important objective marker in rehabilitation. Inertial measurement units may provide an accurate and reliable method of joint angle assessment. The objective of this study was to assess whether a single sensor with the application of machine learning algorithms could accurately measure hip and knee joint angle, and investigate the effect of inertial measurement unit orientation algorithms and person-specific variables on accuracy.

Methods: Fourteen healthy participants completed eight rehabilitation exercises with kinematic data captured by a 3D motion capture system, used as the reference standard, and a wearable inertial measurement unit. Joint angle was calculated from the single inertial measurement unit using four machine learning models, and was compared to the reference standard to evaluate accuracy.

Results: Average root-mean-squared error for the best performing algorithms across all exercises was 4.81° (SD = 1.89). The use of an inertial measurement unit orientation algorithm as a pre-processing step improved accuracy; however, the addition of person-specific variables increased error with average RMSE 4.99° (SD = 1.83°).

Conclusions: Hip and knee joint angle can be measured with a good degree of accuracy from a single inertial measurement unit using machine learning. This offers the ability to monitor and record dynamic joint angle with a single sensor outside of the clinic.

Keywords
Joint angle, wearable sensor, range of motion, inertial measurement unit, biomechanics, machine learning, neural networks

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valid and reliable methods to assess joint angle is imperative.

The current norm in clinical practice is to measure joint angle in a single plane at an isolated joint with a universal goniometer. These are inexpensive and portable and are considered easy to use. However, post-operative joint angle assessment with a universal goniometer can only be captured with a trained examiner when the patient attends clinic appointments. These measurements are often taken several weeks apart, at a single time-point, with a static posture, and do not necessarily provide the data to inform judgement on the overall trend of progress, with measures potentially being affected by short-term pain or swelling. Whilst this method is more accurate than visual estimate, the use of the universal goniometer is subject to high levels of variance in inter and intra-tester reliability.

In an effort to offer a more robust method of measurement, the use of smartphone applications and inertial measurement unit (IMU) systems to measure joint angle has been investigated. Both tools harness data analytics to obtain clinical measurements in an attempt to remove human error. Whilst smartphone applications still require an examiner and static posture to operate, wearable IMU systems have the potential to offer a continuous method of assessment of joint angle remotely during home-exercises, without the need for an examiner or a maintained static posture. Measures of joint angle derived from IMU systems have the potential to be built into biofeedback devices designed to support the patient in their rehabilitation programme away from the clinic.

Current methods of joint angle assessment with IMUs typically require multiple sensors with one IMU per limb segment. At present, it is common to use an orientation algorithm, such as the Madgwick filter, Kalman filter, or complementary filter to compute the IMU orientation of each individual sensor. In the interest of usability and cost, minimising the number of sensors required is preferred; however, there is a lack of research outlining predictive algorithms, or joint angle estimation with a single IMU. A recent study was the first to investigate joint angle measurement with a single IMU. The authors represented joint angle as a Fourier series and optimised a cost function structure using kinematic data, with a mean error of 3.2° across four exercises. However, their method required the input of a number of additional variables including limb segment length data for each participant.

A potential alternative method of joint angle measurement with data from a single IMU is to use machine learning (ML) algorithms. ML algorithms are used widely to find patterns in data and build models to make predictions. This can be done with discrete data, known as classification, or regression, where the prediction output is continuous data, such as joint angle. Supervised learning is one of the two categories of ML algorithms and involves learning a model which best maps input features to labelled outputs. There are wide-varieties of supervised learning algorithms including models such as linear regression, polynomial regression, decision trees, and random forest regression. As such, supervised ML regression algorithms may offer the ability to measure continuous joint angle during rehabilitation exercises captured by IMUs.

To date, the use of ML to assess continuous joint angle captured by IMUs has not been heavily studied. Therefore, the aim of this study was to explore if it is possible to accurately measure joint angle with a single IMU and ML algorithms. This was done by exploring three fundamental questions; (1) which is the best performing ML algorithm to predict joint angle from a single IMU, (2) whether the input of additional anthropometric variables improves the accuracy of such an assessment method, and (3) whether an IMU orientation algorithm is required in addition to ML algorithms to provide this joint angle.

### Methods

#### Participants

A sample of 14 participants (6 female and 8 male, age = 28 ± 3 years, height = 172 ± 9.5 cm, weight = 75 ± 13 kg, BMI 25 ± 4) were recruited from the University. Subjects were eligible to participate in this study if they were over 18 years of age and were capable of performing the eight rehabilitation exercises. Exclusion criteria included: (1) diagnosed neurological conditions and (2) lower limb musculoskeletal injury in the past six months. Ethical approval was obtained from the University Human Research Ethics Committee. All subjects provided written informed consent prior to participation.

#### Rehabilitation exercises

Each participant performed eight lower limb exercises routinely prescribed in the early-stages following orthopaedic surgery under instruction and supervision of a Chartered Physiotherapist. The exercises ranged from lying, sitting and standing positions and were specifically chosen to correspond with standard exercises following total hip and knee replacement surgery. The heel slide, straight leg raise, inner range quadriceps, and seated active knee extension for the knee utilising an IMU on the shin, with supine hip abduction, standing hip flexion, standing hip abduction, and standing hip flexion.
extension for hip rehabilitation, with an IMU placed on the thigh. A detailed description of these exercises can be found in Table 1. Participants were allowed three practice repetitions prior to data collection. All exercises were performed continuously for 60 s. Participants were instructed to vary the joint angle between maximal and sub-maximal repetitions across the set in a self-selected random order.

**Data acquisition**

A three-dimensional (3D) motion capture system, considered the gold standard tool for dynamic measurement of lower limb joint angle with a low error of measurement,7 was used as the reference standard. This CODA motion capture system comprised of a unilateral, right-sided, eight marker set-up, and three motion capture cameras (Charnwood Dynamics, Leicestershire, UK). Two IMUs were used to collect tri-axial accelerometer and gyroscope data from each participant (Shimmer, Dublin, Ireland).33 and all knee rehabilitation exercises were analysed with data solely from the shin sensor (Figure 1: IMU 2), with the thigh sensor being used for hip joint angle measurement (Figure 1: IMU 1). Additional variables including sex, age, height, weight, hip-knee length and ankle-knee length were also recorded. These additional metrics were included to account for variances in joint angle between participants attributed to anthropometric variability. Each participant was required to wear a pair of skin tight Lycra shorts or leggings and a light shirt rolled up past the navel in order to obtain an unobstructed view of all testing equipment. The markers and IMUs were then applied by the same Chartered Physiotherapist for all subjects and were positioned as described in Figure 1. The markers and IMUs were fixed to the skin, or Lycra, with double-sided adhesive tape. Synchronous kinematic data acquisition was conducted using three CODA mpx1 units sampling at 100 Hz and the two IMUs, calibrated prior to testing, sampling at 102.4 Hz, with accelerometer and gyroscope ranges configured to ±2 G and ±500°/s, respectively, mirroring the configuration of similar research.34,35 3D motion capture data acquisition was performed with a single CODA motion analysis system, while IMU data were captured using the Multi Shimmer Sync Android tablet application (Shimmer, Dublin, Ireland). Both systems recorded 60 s segments of continuous kinematics during eight post-operative rehabilitation exercises. A set of exercises was only

| Exercise                   | Description of exercise                                                                 | Joint angle measured | IMU placement |
|----------------------------|----------------------------------------------------------------------------------------|----------------------|---------------|
| Heel slide                 | In supine lying, the exercise is performed by flexing the hip and knee to slide the foot closer to the ipsi-lateral hip. | Knee flexion        | Shin          |
| Supine hip abduction       | In supine lying, the exercise is performed by abducting the hip, sliding the foot away and then back towards the midline. | Hip abduction       | Thigh         |
| Straight leg raise         | In supine lying, the exercise is performed by flexing the hip, lifting the leg off the supporting surface while keeping the knee in full extension. | Hip flexion         | Shin          |
| Inner range quadriceps     | In supine lying, a roll is placed under the knee to be exercised. The exercise is performed by contracting the quadriceps muscles to bring the knee from a position of slight flexion into full extension. | Knee flexion        | Shin          |
| Seated active knee extension| In sitting with the upper thigh supported on a chair, the exercise is performed by contracting the quadriceps to bring the knee from a position of flexion into full extension. | Knee flexion        | Shin          |
| Standing hip flexion       | In standing, the exercise is performed by lifting the leg forwards, flexing at the hip and knee. | Hip flexion         | Thigh         |
| Standing hip abduction     | In standing, the exercise is performed by lifting the leg out to the side, whilst maintaining full knee extension. | Hip abduction       | Thigh         |
| Standing hip extension     | In standing, the exercise is performed by lifting the leg backwards out behind the body, whilst maintaining full knee extension. | Hip extension       | Thigh         |

IMU: inertial measurement unit.
repeated when the CODA marker visibility was less than 99% for any of the eight markers.

**Data processing**

*Reference joint angle calculation.* The CODA system provided raw data in the form of the X, Y, Z positions of each of the markers over time. These 3D co-ordinates were first reduced to 2D, based on the plane of movement the exercise occurred, in order to derive clinically relevant metrics which are already used in current practice (e.g. heel-slide movement is in the Y-Z plane, supine hip abduction is in the X-Y plane and standing hip abduction is in the X-Z plane). Vectors were created from the two markers on each limb involved in the exercise movement and joint angles were calculated using equation (1). The method of calculating the joint angle based on vectors from the CODA system is shown in equation (1).

\[
\theta = \cos^{-1}\left( \frac{\hat{u} \cdot \hat{v}}{\|\hat{u}\| \|\hat{v}\|} \right)
\]  

(1)

*Synchronisation of the motion capture and IMU systems.* Prior to synchronisation, the IMU data were down-sampled to 100 Hz using linear interpolation. To synchronise the systems, the participants were instructed to perform a “kick” before exercise commencement. The kick was performed in a perpendicular plane to the exercise plane, so that the marker’s largest displacement over the duration of the exercise in the

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**Figure 1.** Infra-red markers 1–8 and IMUs 1 and 2 attached with double-sided adhesive tape to anatomical landmarks. Each marker is attached to a battery pack. Only one IMU was used to calculate joint angle, the location dependent on the exercise performed.
perpendicular plane was during the kick. For the CODA system, the joint angle in the direction of the kick was calculated using equation (1), and for the IMU data the IMU orientation in relation to the global frame was computed by using the Madgwick orientation algorithm.\textsuperscript{20} These two data sources were then synced on the peaks of the respective kick data (Figure 2).

**IMU joint angle calculation.** Data from a single IMU were used to measure joint angle as specified in Table 1. Two methods were used to calculate the joint angle from the IMU raw data which are highlighted in Figure 3. Method 1 derived joint angle from the raw IMU data passing through an orientation algorithm which is regularly used in literature pertaining to exercise analysis with IMUs,\textsuperscript{20} whereas Method 2 modelled joint angle straight from the raw IMU data. Four commonly used ML regression algorithms were modelled on the IMU datasets from each of these methods to estimate joint angle, namely linear regression (LR), polynomial regression (PR), decision tree regression (DT), and random forest regression (RF). This culminated in a total of eight models to estimate joint angle from the IMU data (Figure 3). The additional anthropometric variables of height, weight, age, sex and limb segment length were used as additional features to investigate their influence on accuracy. These additional variables particular to each participant were included in the models as part of the feature vector for each timepoint.

**Hyperparameter tuning.** In order to optimise the accuracy of a ML model, a number of parameters that cannot be learned through the ML training process (known as hyperparameters) must be selected before initial training takes place. These hyperparameter values are then adjusted, in this case through manual search, over multiple train and test iterations to identify the optimal model configuration, which is then used for analysis. In this study, L2 penalty coefficient values were explored for the linear regression and polynomial regression, with the polynomial regression model also searching cubic and quadratic features. The decision tree and random forest models searched for the optimal maximum depth value, with estimator values also trialled in the random forest model.

**Accuracy analysis.** The loss metric for all of the models was mean squared error. The root-mean squared error (RMSE) and the coefficient of determination ($R^2$) were computed to compare the predicted joint angle from the IMU to the reference 3D-motion capture system across every data point (Figure 4), for each of the four ML models in all eight exercises. Leave-one-subject-out cross validation was used with 14 folds, and the RMSE values stated in the results are the mean
Figure 3. Flowchart illustrating the process of IMU joint angle calculation. The input label for the training of the models is the raw IMU values, with the output being the joint angle derived from the reference standard CODA.

Figure 4. Randomly selected sample of one participant illustrating joint angle comparison between reference standard CODA and IMU. RMSE was calculated across every data point in the exercise set sampled at 100 Hz for each participant.
Results

Table 2 illustrates the best performing algorithm, average RMSE and R² across all participants for each exercise. The average RMSE for the best performing algorithm across all eight exercises was 4.81° (SD = 1.89), with a maximum value of 6.19°. This increased to 4.99° (SD = 1.83), with a maximum of 6.92° when participant-specific additional variables were included. There was variance between the best performing algorithm dependent on the exercise being conducted, although the use of the orientation algorithm improved performance on the majority of the tested models (11 out of 16).

For clinical relevance, the mean RMSE and R² for the maximum and minimum joint angles of each exercise repetition are also outlined in Table 2. The average RMSE for these joint angles across all eight exercises was 5.02° (SD = 1.99), with a maximum value of 6.79°, resulting in an average increase of 0.21° (SD = 0.54) from the entire time-series. When participant-specific additional variables were included, the RMSE increased to 5.43° (SD = 2.07), with a maximum of 7.41°, resulting in an average increase of 0.44° (SD = 0.46) compared to every data-point.

Discussion

The aim of this study was to investigate whether it is possible to use a single IMU with ML algorithms to accurately measure lower limb joint angles, and which algorithm is most effective in doing so. Furthermore, it explored whether additional anthropometric variables were required to improve the accuracy of such a method, and whether an IMU orientation algorithm was required in addition to the ML methods to provide this joint angle. The results identified low levels of RMSE which suggest that it is possible to measure joint angle with a single IMU with the assistance of a variety of ML algorithms. Additional variables such as sex, age and limb segment lengths reduced the accuracy of this method.

In this study, the best performing ML algorithm with solely the input of sensor data from a single IMU to measure joint angle resulted in an average RMSE of 4.81° using leave-one-subject-out cross validation. These results indicate that the novel approach
described in this paper is comparable to those using two sensor models and a recently published single IMU method. Bakshi et al.\textsuperscript{11} used a two-IMU model to assess knee joint ROM with errors ranging from 0.08 to 3.06\degree across four tasks.\textsuperscript{11} In this method, validation was performed by a single participant and data down-sampled to 5 Hz. Another two sensor method published by O’Donovan et al.\textsuperscript{36} measured ankle joint angle with an error range from 0.5 to 4.09\degree in two subjects.\textsuperscript{36} Bonnet et al.\textsuperscript{26} is the only other study in the current literature to use a single sensor method, although this required the input of all anthropometric variables.\textsuperscript{26} The authors reported an average RMSE of 3.2\degree across four exercises with their single sensor model. However, it is unclear what validation process was used to calculate these accuracy metrics. Finally, the low RMSE identified in this study is also comparable to those found in functional tasks such as gait.\textsuperscript{13,17,18,26} Yet these joint angles do not necessarily mirror the standardised joint angle assessment methods that would be familiar to healthcare professionals in clinical practice.

In a clinical setting, it is desirable to minimise any additional input that a user would be required to perform in order to use this method of measurement. Overall, the addition of anthropometric variables to these models does not appear to increase accuracy. This has positive implications for the ease of implementation, as users will not be required to add further information including measuring limb segment length. Although the addition of person-specific variables is not required to improve accuracy, it is apparent that the use of an IMU orientation algorithm is still necessary, with few models evaluated performing better with raw IMU data.

When viewing the randomly selected sample in Figure 4, there is a suggestion that the model may be less accurate at the end of ranges of each exercise repetition. As clinicians are particularly interested in these end ranges, it is important to conduct further accuracy analysis on these points. The results show that there is a small increase in error at the maximum and minimum joint angle, with mean RMSE at 5.02\degree. However, this is only an average 0.21\degree increase from the full time-series and does not substantially affect the accuracy of the models, providing the clinician with a convenient method of measurement within five degrees of the gold standard.

Further clinical implications of using such a method of joint angle assessment include negating the need for an examiner to perform measurements, therefore removing any error from inter-tester reliability or incorrect placement of the universal goniometer.\textsuperscript{1,4,37} This method of assessment can also offer real-time dynamic joint angle feedback, compared to current methods of goniometry requiring a static position. Whilst other proposed methods are also able to complete this, to the best of the authors’ knowledge, none have been able to do this with a single IMU without the need for limb segment length features to be inputted.

The sensor placement has also been carefully considered for the target user to position appropriately without assistance. Similar work has used sensors on the distal shank or multiple sensors,\textsuperscript{11,14,17,18,26} whereas this system is designed for all of the hip rehabilitation exercises to work with an IMU placed on the thigh, as currently many users may be prevented from reaching below the knee, particularly after total hip replacement.\textsuperscript{38} The knee rehabilitation exercises have an IMU located at the midpoint of the shin, ensuring that users are able to place the sensor easily and maintain the same position for all exercises, although in both cases, further ‘real-world’ validation is required to ensure that IMU placement by untrained patients does not detract from accuracy.

This study is not without its limitations. Results are based on a sample of convenience of young healthy adults in a highly controlled lab-based environment with all placements of markers and IMUs performed by an experienced therapist. Participants were required to wear Lycra shorts and therefore there is the possibility of minor movement from the markers during the exercise. The exercises performed and joint angles measured are relatively early-stage rehabilitation exercises, with motion primarily in a single plane from a standardised starting position, as is usual practice. However, this method may not be applicable to more complex multi-planar functional movements such as in gait or compound lower limb exercises. Finally, some data during two exercises were excluded due to technical difficulties, with suspected issues with the marker battery packs leading to unreliable data from the 3D motion capture system.

This work mirrors numerous previous studies that have included RMSE as the loss metric,\textsuperscript{17,19,26,36} which is common in assessing the accuracy of regression tasks. However, there is some debate in the literature regarding the most appropriate indicator of average model performance and, it is suggested that a combination of metrics including RMSE and mean absolute error are required to assess model performance.\textsuperscript{39,40} The use of RMSE does not necessarily provide an indication of whether systematic errors are present in the model, or the precision of the model over a given time period. Therefore, while this study has shown potential for ML methods to measure joint angle, further in-depth evaluation should be carried out on unseen and uncontrolled data in order to determine the validity, reliability (inter- and intra-person) and minimum detectable changes of the proposed model.
These limitations aside, the results from this study suggest future work that can incorporate this novel method of joint angle assessment into an exercise biofeedback system that can be used in the home-setting, providing continuous joint angle measurement with remote monitoring for the clinician. This would also offer clinicians a reliable and dynamic method of assessing joint angle in the clinic which removes any examiner-based error. Additionally, future work should include validating this method in a clinical population with sensor placement performed by the participant, as well as building on the training data used in this study with data from a wider participant demographic. Finally, having shown the potential of this method of joint angle measurement, an interesting field of future work is to compare the accuracy of this single IMU ML model with the traditional multi-IMU approaches discussed in the wider literature.

Conclusions

This study illustrates a novel and effective method of measuring joint angle across numerous exercises using only a single IMU, with a good level of accuracy when compared to the gold standard. This model is designed to maximise ease of clinical implementation as it reduces the need for patient-specific features such as limb segment length, sex and age to be input into the model. This has potential to be built into an exercise biofeedback platform to offer an accurate and dynamic method of joint angle assessment outside of the clinic, without the need for a trained examiner.

Declaration of conflicting interests

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Guarantor

RA.

Contributorship

RA and SD are co-lead authors. RA proposed the concept in liaison with SD and BC. The study was designed by RA and SD. Recruitment was performed by RA. Data collection was carried out by RA, SD and AR with RA, SD and MOR carrying out data analysis. BC provided supervision throughout. Original draft was prepared by RA, SD and AR with review and editing from MOR and BC. All authors read and approved the final manuscript.

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Research ethics and patient consent

Ethical approval was obtained from the University College Dublin Human Research Ethics Committee – Sciences (HREC-LS). This study was deemed to be exempt from full ethical review (Ref: LS-E-18-76-Argent-Caulfield). All participants provided written informed consent prior to participation.

Data

The datasets generated and/or analysed during the current study are available in the Zenodo research data repository, [www.zenodo.org].

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