Magnetic Phase Diagram of Li$_2$(Pd$_{1-x}$Pt$_x$)$_3$B by AC Susceptometry

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The $H$–$T$ phase diagram and several superconducting parameters for Li$_2$(Pd$_{1-x}$Pt$_x$)$_3$B have been determined as a function of cation substitution $x$. Notably, the coherence length may be linear in platinum concentration. Despite the superconducting pairing state and band structure apparently changing fundamentally, the $H$–$T$ phase diagram is essentially unchanged. Unusual aspects of the shape of the $H$–$T$ phase diagram are discussed. The upper critical field $H_c(0)$ is not anomalously high for any Pt content, likely due to an absence of high carrier masses — in such a case, the value of $H_c(0)$ would not serve as a probe for novel physics.

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I. INTRODUCTION

Most superconductors have crystal structures containing an inversion center, such that transposing every atomic position through that point returns the original crystal structure. In such a superconductor, parity constrains the superconducting pairing state to be either singlet or triplet, and the basic physical properties of this state, if not always the underlying mechanisms, are well-known. However, noncentrosymmetric superconductors, those which lack spatial inversion, also exist, and such materials can exhibit extremely unconventional behavior. The first indication of novel physics in such a system was in CePt$_3$Si$_2$ which was found to have an extremely high, non-Pauli-limited upper critical field $H_{c2}$. This touched off strong interest in noncentrosymmetric materials, with systems as diverse as UIr$_2$B-doped SiC$_x$Mo$_3$Al$_2$C$_x$ Mg$_{10.5}$Ir$_{19}B_{17.1}$ and 1-1-3 silicides such as CeRhSi$_3$, BaPtSi$_3$, or CaIrSi$_3$ being studied. A non-Pauli-limited $H_{c2}$ remains a key signature of novel behavior in noncentrosymmetric superconductors.

In the absence of inversion symmetry, parity is no longer a meaningful concept, and the pairing state can thus no longer be strictly classified as singlet or triplet. Spin-orbit terms that otherwise cannot contribute due to symmetry can split the band structure and Fermi surface by spin orientation. This can lead to a spin imbalance at the Fermi surface and, if the splitting is large compared to the superconducting gap, to pairing that is largely constrained to be within each Fermi-surface sheet, implying an admixture of singlet and triplet components. While much theoretical work remains to be done on these materials, a remarkable array of exotic phases and responses have been predicted, from unusual magnetoelectric effects to FFLO-like pair density wave states with spatially-varying pairing functions, states with helical nodes around vortices, or states with half- or quarter-quantum vortices, in the presence of a small magnetic field.

Perhaps since most of the exotic effects arising from the lack of spatial inversion require that the bands exhibit significant spin-orbit splitting at the Fermi surface, the majority of the noncentrosymmetric systems studied to date have been found to behave in a fairly conventional manner. Indeed, unusual behavior has been reported almost exclusively in heavy-electron lanthanide and actinide systems, and a great deal of the predicted physics remains unobserved. By far the clearest evidence for unconventional behavior without heavy electrons is in Li$_2$(Pd$_{1-x}$Pt$_x$)$_3$B, which appears to be fully gapped and singlet-dominated for $x = 0$ but exhibits line nodes and strong triplet character for $x = 1,15,19$ with indications of unconventional behavior as early as $x = 0.2$. Given this rather fundamental change in behavior with cation substitution, and noting that the most unusual consequences stemming from the lack of inversion are manifested in the magnetic properties, a detailed magnetic phase diagram for the substitution series would be of interest. Indeed, the shape of the upper critical field as a function of temperature may indicate the dominant pairing symmetry and the strengths of various interactions in these materials, and several predictions have been made for the $H$–$T$ phase diagram. While portions of an $H$–$T$ phase diagram have been reported for several substitution levels based on $M$–$H$ loops, it was not possible to resolve the shape or especially the low-temperature behavior, and a lack of low-temperature points made extrapolation to a reliable $H_{c2}(0)$ difficult. The primary purpose of this paper is to provide the full substitution dependence of the magnetic phase diagram.

II. EXPERIMENTAL

Polycrystalline ingots of Li$_2$(Pd$_{1-x}$Pt$_x$)$_3$B were prepared from Li (99.9% purity), Pt (99.999%), Pd (99.95%), and B (99.8%) by a two-step arc melting process, with a slight excess of lithium used to compensate for losses due to evaporation. Pieces mechanically sep-
Figure 1 shows the temperature dependence of the ac susceptibility of a Li₂(Pd₁₋ₓPtₓ)₃B sample with x = 0.20. The narrow transitions indicate good homogeneity and sample quality. After some initial broadening in very low fields, the width changes little until very close to \( H_{c2}(0) \), at which point the transitions broaden rapidly. The decrease in transition temperature with field appears to be fairly constant over much of the phase diagram. No unusual glitches or secondary transitions are observed that would suggest the presence of additional phase transitions, although small peaks just below the superconducting transition, attributed to depinning of the vortex lattice, were observed in some samples when they were warmed after rapid cooling (not shown).

**III. RESULTS AND ANALYSIS**

![Graph showing temperature dependence of ac susceptibility](image)

**FIG. 1.** (color online) Temperature and field dependence of the diamagnetic shielding \( \chi'_{ac} \) (negative) and loss \( \chi''_{ac} \) (positive) for Li₂(Pd₁₋ₓPtₓ)₃B with x = 0.20.

Figure 2 shows example \( H-T \) phase diagrams derived from such data, for x = 1 (the Pt endmember) and x = 0.20. The upper critical field is indeed remarkably linear over much of the phase diagram, then turns over rapidly at high fields. Transitions extracted from specific heat data are included for comparison — the shape is similar, but the slope is higher. The near-agreement confirms that the measured \( \chi_{ac} \) is bulk-sensitive. Areas where the \( \chi_{ac} \) data fall below the \( \chi_{el} \) points could indicate a vortex liquid state, in which field penetrates the sample almost completely and the vortices are mobile, mimicking normal-state response to ac stimulus. However, since the polycrystalline samples had irregular shapes, their mi-
crostructure is unknown, and their orientation was most likely not the same in both experiments where the same sample was used, it is also quite possible that this difference is attributable to grain structure or demagnetizing effects. It should also be noted that, in the Pt endmember at least, pinning has been found to be extraordinarily strong.24

Despite the unconventional behavior observed in the Pt endmember by other techniques, the high, non-Pauli-limited $H_{c2}$ generally associated with noncentrosymmetric physics is not observed. Preliminary specific heat data on the samples studied here and previous reports in this system25,27,28 all indicate a normal-state electronic specific heat coefficient $\gamma_n$ of about 7–10 mJmol$^{-1}$K$^{-2}$, consistent with ordinary $d$-electron metals. In order to see Pauli depairing, it is necessary that orbital effects not break the pairs first. In systems such as CePt$_3$Si, heavy Fermion masses lead to a suppression of orbital pair-breaking effects, and the absence of Pauli pair breaking is clear. In Li$_2$(Pd$_{1-x}$Pt$_x$)$_3$B, however, orbital limiting is not suppressed, and $H_{c2}$ may not probe Pauli limiting effects. Thus, while no anomalously high $H_{c2}$ is observed, this should not be taken as evidence for an absence of novel physics.

The shape predicted for $H_{c2}(T)$ in the WHH dirty limit calculations27,28 based on BCS theory, is also shown in Fig. 2 for each sample. This curve is most commonly used to predict an approximate value of $H_{c2}(0)$ from $T_c$ and $dH_{c2}/dT|_{T=T_c}$ when the data do not allow extrapolation to zero field. For the purposes of the comparison in Fig. 2 the main slope rather than the initial slope was used, due to curvature near $T_c$ which is in clear violation of WHH expectations (see inset for $x=0.20$) and may not represent intrinsic behavior. Even neglecting the lowest fields, the WHH curve fails to fully capture the shape of $H_{c2}(T)$. Within a conventional picture, this could possibly be understood in terms of a breakdown of one or more assumptions underpinning the WHH calculations, for instance by multi-band or strong-coupled superconductivity.

A variety of predictions have been made for $H$–$T$ phase diagrams in noncentrosymmetric systems12,14,21 but these curves generally exhibit strong downward curvature near $T_c$ and do not capture the other essential features of the $H$–$T$ phase diagrams reported here. The general case in the presence of impurities, however, cannot be solved analytically, and the results are strongly dependent on fine details of the band structure, pairing symmetry, and intra- and interband coupling.29

The $H$–$T$ phase diagram is shown as a function of cation substitution in Fig. 3. Since the Pt and Pd endmembers have very different band structure26 and since replacing Pd by Pt introduces nodes in the gap25 and changes the NMR Knight shift and $1/T_1$, from singlet-to triplet-like behavior19,31 one might expect significant changes in the $H$–$T$ phase diagram. This is not observed. The shape of the $H$–$T$ phase diagram changes little with Pt content. All curves exhibit upward curvature near $T_c$, are remarkably linear over much of the field range, then curve over rapidly at high fields.

To check for the presence of any evolution with cation substitution, Fig. 3 plots all the $H$–$T$ phase diagrams together, scaled by $T_c$ and $H_{c2}(0)$. While the data for different Pt contents do not collapse perfectly onto a single curve, no systematic evolution can be discerned. Given the fundamental changes in the nature of the supercon-
ducting state and the differences in the band structure, this degree of uniformity from one end of the substitution phase diagram to the other is particularly striking.

![Graph](image)

FIG. 5. Transition in $\chi''_{ac}$ for very low dc fields, $x = 0.20$ ($\mu_0 H_{c2}(0) \approx 3.24$ T; $H_{ac} = 0.1$ mT rms). The peak grows and broadens, developing a tail to low temperature.

It has been previously pointed out\textsuperscript{22} that upward curvature in $H_{c2}$ near $T_c$ as observed in this compound has also been seen in polycrystalline MgB$_2$ and borocarbides.\textsuperscript{32,33} As very low fields are applied, the transitions broaden, an effect that is most pronounced in the $\chi''_{ac}$ fluctuation peak, the intensity of which also grows markedly (see Fig. 5). This suggests that grain boundary transport is strongly suppressed by field, and that the apparent upward curvature arises from critical current effects at junctions, rather than from entropy. This may also offer an additional explanation for the small suppression of the magnetization-derived $H$–$T$ phase diagram relative to that extracted from specific heat measurements — $c_{44}$ measurements are not sensitive to grain boundary transport.

The substitution-dependence of the transition temperature and the zero-temperature extrapolated upper critical field are presented in Fig. 6(a); the superconducting coherence length calculated from $H_{c2}(0)$ using the relation $\mu_0 H_{c2}(0) = \Phi_0/(2\pi\xi^2_0)$ for orbital-limited fields is shown in Fig. 6(b). The trend observed previously in $T_c$ tracks that previously reported\textsuperscript{21} but with significant deviations on the order of 0.5 K, perhaps due to the system being highly defect-sensitive or to a variable lithium concentration. As might be expected given how little the $H$–$T$ phase diagram changes with cation substitution, the substitution-dependence of $H_{c2}(0)$ takes a similar shape. Perhaps more surprisingly, the extracted zero-temperature coherence length appears to vary linearly with platinum content. A coherence length linear in cation substitution would suggest $H_{c2}(0, x) \propto (x + a)^{-2}$ and, assuming the BCS $\xi_0(x) \propto \hbar v_F/k_B T_c(x)$ to hold and $v_F(x)$ to be approximately constant, $T_c \sim (x + a)^{-1}$. The dashed lines in Fig. 6 represent these power laws, with a taken from $\xi_0$. The significance of the coherence length varying linearly with cation substitution, if any, is not clear, and the possible sensitivity to defects in these materials requires that this result be treated with caution.

![Graphs](image)

FIG. 6. (color online) Dependence of $T_c$, $H_{c2}(0)$ and $\xi_0$ on cation substitution. Diamonds are $T_c$ data from Ref. 22.

IV. CONCLUSION

In summary, the $H$–$T$ phase diagram of Li$_2$(Pd$_{1-x}$Pt$_x$)$_3$B has been determined as a function of $x$, and the substitution-dependence of several superconducting parameters has been elucidated — most notably, the coherence length appears to vary linearly with platinum concentration. Although the superconducting pairing state is thought to change fundamentally, from a fully-gapped, singlet-like to a triplet-dominated form with nodes, and the band structure changes substantially with cation substitution, the $H$–$T$ phase diagram is essentially unchanged. This striking result puts constraints on the changes seen in the pairing state, indicating a continuous evolution where an abrupt change would be expected. Upward curvature near $T_c$ suggests poor transport at grain boundaries, while an abnormally linear, non-WHH shape indicates the superconducting state to be more complicated than simple single-band weak-coupling BCS. The curve does not resemble predictions for noncentrosymmetric superconductors, but the shape expected in such a system can be extremely sensitive to a host of factors, including impurities, pairing symmetry, and fine details of the band structure. The $H_{c2}(0)$ values found in this study are not anomalously high as in CePt$_3$Si and some other materials, but this may be be attributable to an absence of the high carrier masses required to suppress orbital depairing and expose the presence or absence of
Pauli limiting behavior. In such a scenario, the value of $H_{c2}(0)$ would not serve as an effective probe for the presence of novel physics.

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