Distance scaling of electric-field noise in a surface-electrode ion trap

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We investigate anomalous ion-motional heating, a limitation to multiqubit quantum-logic gate fidelity in trapped-ion systems, as a function of ion-electrode separation. Using a multizone surface-electrode trap in which ions can be held at five discrete distances from the metal electrodes, we measure power-law dependencies of the electric-field noise experienced by the ion on the ion-electrode distance $d$. We find a scaling of approximately $d^{-4}$ regardless of whether the electrodes are at room temperature or cryogenic temperature, despite the fact that the heating rates are approximately two orders of magnitude smaller in the latter case. Through auxiliary measurements using the application of noise to the electrodes, we rule out technical limitations to the measured heating rates and scalings. We also measure the frequency scaling of the inherent electric-field noise close to $1/f$ at both temperatures. These measurements eliminate from consideration anomalous-heating models which do not have a $d^{-4}$ distance dependence, including several microscopic models of current interest.

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Trapped atomic ions manipulated using electromagnetic fields are a promising system for large-scale quantum information processing (QIP) [1], but the fidelity of multiqubit operations based on the Coulomb interaction can be limited by ion heating and motional-state decoherence caused by electric-field noise. This noise is observed to be significantly larger in amplitude than the expected thermal (Johnson) noise of the voltage on the trap electrodes and associated circuitry [2,3], and has therefore been termed anomalous. Anomalous motional heating has been suspected, and observed in a few experiments [3–6], to be strongly dependent on the spatial separation between the ions and the electrode surfaces. The reduction of this separation, which results in higher trap frequencies, and thus stronger ion-ion interactions, will be beneficial for increasing the speed of trapped-ion quantum logic based either on optical [7–9] or magnetic-field-gradient [10] excitation. Additionally, high-rate, high-fidelity ion-state readout across an array can be enabled by trapping ions close to detectors integrated into trap chips [11,12]. It is therefore of paramount importance to carefully determine how electric-field noise varies with ion-electrode distance $d$ in potentially scalable systems.

Theories put forth to explain anomalous heating suggest power-law scalings of the electric-field spectral density (proportional to the heating rate) of $d^{-\beta}$ with the heating-rate exponent $\beta$ in the range of $0–8$ [13]. An early model suggested to explain anomalous heating depends on small “patches” of the electrode surface, each with different electric properties, such as the local work function, that lead to contact potentials between the patches, and therefore a spatial electric-field variation above the surface [2]. The time variation of these potentials due to thermal noise or other excitation can lead to ion heating. For patches small in lateral extent compared to $d$, a scaling exponent $\beta = 4$ is expected [14,15].

While anomalous heating has been observed in many experiments in many types and sizes of trapping structures [13], systematic and uncontrolled variations between experiments, materials, geometries, and techniques have precluded direct comparison to obtain reliable scalings without invoking assumed scalings in other quantities (cf. Ref. [3] in which scaled traps were measured in separate experiments). The few experiments that have been performed to explore this scaling in a single device or experiment have been performed either using trap geometries that are not easily scalable [4,5], which may limit their technological relevance for QIP, or in the limit of high ion temperature [6] with potentially limited bearing on the few-motional-quanta level required for high-fidelity quantum logic. The temperature dependence of the exponent, which may help elucidate the underpinnings of electric-field noise, is also currently unknown in a trapped-ion context.

Here, we measure the dependence of anomalous heating on ion-electrode separation in a single trap with multiple zones of varying trapping distances. We use a surface-electrode design [16], which has great potential for scaling to large arrayed structures while employing integrated control and readout technologies required for large-scale QIP [17,18]. We measure heating rates from the ground state of the ion’s motion in the trap potential using the motional-sideband-ratio [19] and Rabi-flopping [20] techniques, robust methods for measuring heating in the low-excitation (few-phonon) limit that assume only a thermal motional state of the ion. We measure the noise as a function of $d$, and as a function of frequency at one value of $d$, for two electrode temperatures, 295 and 5 K. We observe that the distance and frequency scalings are independent of temperature. Additionally, we apply voltage noise to the electrodes to verify that the nominal heating-rate scaling is not due to technical noise (i.e., noise from pickup
in the wires or generated by the sources and circuitry used to apply potentials to the electrodes). We observe a different, expected distance dependence of heating in this circumstance, suggesting that the intrinsic noise appears to originate from the electrode surface itself.

We employ a surface-electrode trap made from a 2-μm-thick sputtered niobium electrode layer deposited on a sapphire substrate. Electrodes were defined in the metal film via optical lithography and plasma etching. The electrode design creates a linear Paul trap of varying ion-surface distance in five different zones along the trap axis (cf. Fig. 1). The ion-surface distance is determined by the lateral size and spacing of the radio-frequency (rf) electrodes in this structure [21,22], and the five zones produce trapping minima at nominal ion-surface separations of 83, 64, 49, 38, and 29 μm. The uncertainty in d is approximately 1 μm, primarily due to trap potential simulation precision [23]. Ions can be trapped in all of these zones using a combination of rf fields and static potentials applied to subsets of the segmented control electrodes that axially define each zone. The rf voltage was changed for each trapping zone, while keeping the axial frequency the same. The trap depths ranged from 0.05 to 0.08 eV.

For heating-rate measurements, a single $^{88}$Sr$^+$ ion is held in one of these five zones, and laser beams used to cool, manipulate, and read out the ion’s electronic state are directed parallel to the trap surface, focused on the ion. The trap is housed in a cryogenic vacuum system (described previously [24]) in which ultrahigh-vacuum conditions can be sustained while the trap chip temperature is maintained at room temperature or 5 K. Loading is accomplished from a two-dimensional magneto-optical trap of neutral strontium atoms remotely located and accelerated to the trap where they are photoionized [25]. Doppler cooling on a strong dipole-allowed transition and resolved-sideband cooling on the optically addressed $^2S_{1/2} \rightarrow ^2D_{5/2}$ transition bring the ion to the ground state of the axial mode of vibration in the trap. Sideband spectroscopy [19] or carrier Rabi flopping [20] on the optical transition is then used to measure the axial-mode ground-state occupation after varying postcooling delays.

Sideband spectroscopy, where the mode occupation is determined from the ratio of the red and blue motional-sideband amplitudes, is used for all measurements except the room-temperature distance scaling. In the former case, the ground-state occupation probability was typically >0.95 after sideband cooling. In the latter case, the Rabi-flopping technique, where the mode occupation is determined by fitting electronic-carrier-transition Rabi-flopping curves, was used due to the lower uncertainty of this method for higher motional excitation (a few to $\sim$10 phonons; here, for the highest heating rates, the initial mode occupation was $\hbar < 2$). We crosschecked the two methods against each other and see general agreement, with the Rabi-flopping method producing systematically higher heating-rate values by 30%, consistent with previous work [26]. As the entire distance scaling data set at 295 K was taken in this manner, the analysis of the scaling exponent of the heating rate is insensitive to this systematic uncertainty in measurement, giving us confidence in the exponent at much better than the 30% level, ultimately limited by statistical uncertainty in the measurements.

For these experiments, we employ low-pass filtering below the trap frequency on all control electrodes. Additionally, we bandpass filter the applied rf signal and, in every trap zone, we compensate stray fields so as to minimize the pseudopotential gradient along the axial direction and thus eliminate heating from noise near the rf frequency [27,28]. We have observed that this method is sufficient to locate the ion at the rf null in the radial directions with an uncertainty in the vertical direction of 1 μm.

To determine the scaling of electric-field noise with $d$, we performed measurements of the heating rate at a fixed axial frequency of 850 kHz in different trap zones. (The behavior of the ion in the 29-μm zone when the chip was at a temperature of 5 K was atypical, leading us to believe uncompensated stray fields were often present in this circumstance; we therefore did not obtain heating-rate data for this case.) These data are plotted in Fig. 2 for 295 and 5 K chip temperatures. While the overall heating rates are $\sim 100 \times$ smaller at 5 K than at 295 K, the distance scalings are the same within error, with values of $\beta$ of 3.9(2) and 4.0(2), respectively, where the number in
the heating rate thus gives the frequency scaling of lar frequency (measured in one zone (models. The frequency dependence of the ion heating rate was source due to the different dependencies predicted by particular heating rate can also aid in determining the electric-field noise uncertainties in the heating rates as propagated through the sideband-ratio measurements.

parentheses is the standard uncertainty in the last digit. We note that the niobium electrode metal is superconducting at 5 K, and the heating-rate scaling is therefore unchanged above and below the transition temperature \( T_C \); the insensitivity to bulk superconductivity is not unexpected in light of previous data, demonstrating no significant difference in heating-rate amplitude just above and below \( T_C \) [24,29].

Measurement of the frequency dependence of the ion heating rate can also aid in determining the electric-field noise source due to the different dependencies predicted by particular models. The frequency dependence of the ion heating rate was measured in one zone \( (d = 64 \, \mu m) \), by varying the axial trap frequency, at both room and low temperature; these data are presented in Fig. 3. The heating rate \( \dot{\tilde{h}} \) is proportional to the electric-field spectral density \( S_E(\omega) \) as

\[
\dot{\tilde{h}} = \frac{e^2}{4\hbar\omega_0} S_E(\omega).
\]

Here, \( e \) and \( m \) are the ion’s charge and mass, respectively, \( \hbar \) is the reduced Planck’s constant, and \( \omega \) is the trap angular frequency \((=2\pi f, \text{ for frequency } f)\). Measurement of the heating rate thus gives the frequency scaling of \( S_E(\omega) \). We observe frequency scalings of the electric-field spectral density as \( f^{-1.4(2)} \) and \( f^{-1.8(2)} \) at room and low temperature, respectively. This is consistent with the \( 1/f \)-like frequency dependence seen in several other experiments [13], and the fact that it is unchanged over this temperature range suggests that the mechanisms responsible for heating at high and low temperature are similar or related. The observed distance scaling also supports this interpretation.

In the regime where technical noise or Johnson noise dominates, the heating rate should scale as \( \sim 1/D_{ij}^2 \) [30], where \( D_{ij} = V_j/E_i \) is the characteristic distance of electrode \( j \) for fields along direction \( i \) at the ion location, where \( V_j \) is the voltage applied to electrode \( j \), and \( E_i \) is the resulting electric field along direction \( i \) at the ion position. In the multisegment, variable-height trap we use here, characteristic distances for electrodes seen by the ion in each of the zones do not directly correspond to the ion-electrode distances \( d \) in those zones, as the staggered shape of the rf electrodes, the lack of constant scaling of all dimensions of the electrodes among zones, and the presence of connected control electrodes of differing sizes in neighboring zones affect, in a nonsymmetric manner, the field produced by each electrode. Through boundary-element-method potential simulation of our trap, we have calculated these characteristic distances and their effect on distance scaling. For technical or Johnson noise on the electrodes, including electromagnetic pickup, these characteristic distances lead to an expected approximate-power-law scaling exponent \( \beta = 2.4(3) \) when considering the ion-electrode distances used here. The difference from perfect power-law scaling, here quantified as an uncertainty in the exponent, is due to the unequal scalings of the electrode axial dimensions among zones. Uncertainty in the ion’s position \((\sim 1 \, \mu m)\) leads to an expected heating-rate contribution uncertainty correlated to this position.

To experimentally investigate the distance scaling of injected noise, we follow a procedure outlined briefly here; it will be described in detail in a future publication [27]. White noise, over a 10 Hz to 2 MHz range and at a level >40 dB...
higher than the intrinsic noise measured on the leads going to the control electrodes, is injected onto a pair of electrodes that are connected electrically on the chip (some electrodes are shared between zones to minimize required leads; cf. Fig. 1). The contribution to the heating rate from externally injected noise is determined for each zone, accounting for \(\sim 5 \text{ kHz} \) single-pole low-pass filters near the chip. In Fig. 4, we plot the results of this measurement along with the scaling determined from the calculated characteristic distances. As can be seen, the measured heating-rate scaling of \(\beta = 2.5(3)\) is equivalent to the expected scaling within error, and is significantly different from the value \(\beta = 3.9(2)\) observed without noise injection. Simulations considering uncorrelated noise independent of voltage on each electrode show an expected behavior of \(1/d^{2.43}\), while simulations for correlated noise on each electrode predict a scaling of \(1/d^{3.0(3)}\). This confirms that the scaling measured without injected noise is not limited by technical or Johnson noise, nor by pickup within the chamber, for the noise models considered here. We also note that the measured distance scaling without injected noise eliminates blackbody radiation (BBR) as a limiting source of electric-field noise; close to an electrode surface, BBR will lead to a heating rate with scaling exponent \(\beta\) in the range of 2–3 [13].

The measured distance scaling puts limits on theories proposing microscopic origins of anomalous heating, assuming that the mechanism for heating is the same in each site. A general patch potential model, agnostic to the mechanism within the patches, predicts \(\beta = 4\) for patches much smaller than \(d\), consistent with what is seen here [13–15]. Our data are thus consistent with a patch size much smaller than \(~30 \mu\text{m}\), therefore eliminating electrode- or chip-sized patches, i.e., uniform fluctuations on a large scale, for which one would predict \(\beta = 2\). We expect the crystalline grains in the polycrystalline sputtered niobium film in which the electrodes are defined to be not larger than 200 nm in size (\(\ll d\)), but it is not possible to verify that these grains correspond to patches without making measurements at much smaller \(d\).

The adatom diffusion model [2,13] predicts \(\beta = 6\) for noise measured parallel to the surface of planar electrodes, and thus would appear to be eliminated over the entire temperature range; this is true also for extensions that depend on diffusion between small patches that allow for spatiotemporal variation in induced dipole moments [13,31].

Models with adatom dipoles that fluctuate in size [32] predict \(\beta = 4\) as seen here, but the frequency scaling of the noise expected in this case is flat, corresponding to \(f^{-1}\) scaling for the heating rate by Eq. (1), inconsistent with the scaling seen here at both temperatures, and with almost every other measurement citing a frequency scaling [13]. Two-level fluctuators (of which adatom dipoles are potentially a subset) have also been suggested [13,33], particularly in light of their potential relevance to electronic noise in conductors and \(1/f\)-type predictions. This model also predicts \(\beta = 4\) for planar electrodes, and so is consistent with all the data presented here. This model is, however, not supported by more extensive measurements of temperature and frequency scaling [34,35].

One model that is consistent with the measurements performed here is based on lossy dielectric films atop the electrodes [36]. This model predicts electric-field noise proportional to \(1/f\) and to temperature as \(T\), with \(\beta = 4\). There is also dependence on the loss tangent and dielectric constant of the thin film, properties whose frequency and temperature dependence could lead to the overall dependencies seen previously (e.g., Ref. [35]). We also have evidence from x-ray photoelectron spectroscopy of fabricated traps that thin layers of dielectric materials, namely, hydrocarbons and, in some materials, oxides, are present on the electrode surfaces. Further investigation of these film material properties on fabricated trap electrodes, as well as measurements of heating rates as a function of film thickness and composition, is required to more carefully determine the relevance of this mechanism.

The results of a recent room-temperature distance dependence measurement in a gold trap [6] are similar to those observed here in a niobium trap, and the former experiment also measured the heating of an axial mode parallel to the trap surface. Besides lending more support to the conclusions drawn above pertaining to model viability, this also suggests that material insensitivity seen previously in the temperature dependence of electric-field noise [24] is a more general phenomenon, one that any microscopic theory explaining anomalous heating must address. Straightforward comparisons cannot be made to distance scalings measured in Refs. [4] or [5] due to the use of nonplanar geometries.
These results suggest that scaling to smaller trap structures to perform high-fidelity quantum-logic gates at higher rates will indeed be impractical without further mitigation of anomalous heating. As a result, understanding the origins of anomalous ion heating remains of foremost importance. Our measurement of the ion-electrode-distance scaling of electric-field noise strongly constrains proposed models for the microscopic mechanism(s) behind anomalous ion heating. As this scaling appears to be unchanged between 295 and 5 K, a similar mechanism should be suspected at both temperatures; proposed models must support this scaling while also providing for heating-rate values to vary substantially in amplitude over this temperature range. The model based on lossy dielectric layers is still viable, and targeted surface preparation [37–39] and materials characterization in conjunction with careful heating-rate measurements may further elucidate the viability of this or other mechanisms of anomalous ion heating.

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