Vibrational and dielectric properties of the bulk transition metal dichalcogenides

Nicholas A. Pike,1,2,* Antoine Dewandre,2 Benoît Van Troeye,3 Xavier Gonze,3 and Matthieu J. Verstraete2
1Centre for Materials Science and Nanotechnology, University of Oslo, NO-0349 Oslo, Norway
2Nanomat/Q-Mat/CESAM, Université de Liège & European Theoretical Spectroscopy Facility, B-4000 Liège, Belgium
3Université Catholique de Louvain, Institute of Condensed Matter and Nanosciences (IMCN) & European Theoretical Spectroscopy Facility, B-1348 Louvain-la-Neuve, Belgium

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Interest in the transition metal dichalcogenides (TMDs) is widespread in materials science since they display a number of useful properties for industrial and engineering applications [1,2]. Indeed, the bulk electronic properties of these materials vary greatly depending on their chemical makeup and underlying crystal symmetry [3,4]. For electronic and photovoltaic applications these materials display promising features, including an indirect to direct band-gap transition that can be controlled via the number of layers or by the application of strain [2,5–8]. They are known to have high electron mobilities [9–11] and have excellent lubricative properties due to their layered nature. Some of these materials exhibit charge-density waves (CDWs) [12–21]. Several recent high-throughput studies have shown the power of density functional theory to identify materials which can be exfoliated and have useful physical properties [22–24].

Several optoelectronic devices [25–27] have been proposed which contain heterostructures of TMD materials in the hopes of blending their unique properties. The understanding of these heterostructures, either as truly two-dimensional layers of materials or semibulk layered materials, requires detailed knowledge of the mechanical, electronic, dielectric, thermal, elastic, and acoustic properties of the individual components. These properties are intimately linked and a full picture is essential to understand heterostructured systems composed of TMDs and other two-dimensional materials.

To understand the properties of these materials and find trends among them, we undertake an investigation using the same functionals and approximations for a wide range of commonly used TMD materials. Our examination uses density functional theory (DFT) [28] and Density Functional Perturbation Theory (DFPT) [29], where the particular effects of different commonly used approximations are examined. We find that many DFPT properties are strongly dependent on the lattice parameters and on the inclusion of long-range $e^{-} - e^{-}$ correlation, approximated via a van der Waals (vdW) dispersion scheme from Grimme known as DFT-D [30–32].

In Sec. II, a brief outline of the methods used and a brief description of the crystal structures of the compounds investigated here are followed by a discussion of the effects of the different approximations used to calculate the phonon band structures and interatomic force constants where the most important contributions are highlighted. In Secs. III–V, we present the mechanical, electrical, dielectric, thermal, and acoustic properties of three prototypical TMD systems, show their corresponding electronic and phonon band structures, phonon density of states, and Raman spectra, and display global trends and outliers in the properties of the full set of TMDs. The numerical data for all systems is given in the Supplemental Material (SM) [34]. Finally, we summarize and conclude in Sec. VI.

II. CALCULATION METHODS

We employ DFT [28] and DFPT [29,35,36] as implemented in the ABINIT software package [37–39], with a plane-wave basis set and norm-conserving pseudopotentials. For a review of DFT and its role in electronic structure calculations see Ref. [40], and for a summary of DFPT and its role in the calculation of the vibrational properties see Refs. [29,41,42]. More details of our DFT and DFPT calculation parameters for these materials, including energy cutoffs and grid sampling [43], are found in the SM [34]. For our calculations of the
Raman spectra, we assume a fixed Lorentz broadening of the spectral lines of $1.0 \times 10^{-5}$ s and a laser wavelength of 532 nm representing a frequency typically used in Raman experiments [44,45]. The intensity of each Raman spectra should only be used to demonstrate the existence of Raman peaks near the calculated frequencies, as the calculations presented here use the local density approximation (LDA) exchange correlation during the calculation of the third derivative of the total energy with wave functions calculated using a generalized gradient approximation (GGA) exchange-correlation functional and a vDW dispersion correction. Our plotted Raman intensities are also rescaled by its corresponding maximum value, and thus only relative differences in intensity can be compared directly to experiment.

There are three main families of TMDs: hexagonal (h-TMDs) with space group $P6_3/mmc$, trigonal (t-TMDs) with space group $P3m1$, and triclinic (tc-TMDs) with space-group symmetry PT. In Fig. 1 we show example structures for each of the three crystal symmetries, namely, we consider the h-TMDs: MoS$_2$, MoSe$_2$, MoTe$_2$, WS$_2$, WSe$_2$, NbS$_2$, and NbSe$_2$; the t-TMDs: TiS$_2$, TiSe$_2$, TiTe$_2$, and ZrS$_2$, ZrSe$_2$; and finally the tc-TMDs: ReS$_2$, ReSe$_2$, and TcS$_2$. The variety of crystal symmetries found in the TMDs gives rise to unique physical properties, with each material being composed of layers of metal atoms packed between two layers of chalcogen atoms. In the case of the bulk h-TMDs, the unit cell consists of two trilayers containing three atoms per layer. As shown in Fig. 1(a), this leads to a well-known graphenelike hexagonal configuration in the $x$-$y$ plane. The AB stacking between the layers can be clearly identified in the $y$-$z$ plane. For the t-TMDs, shown in Fig. 1(b), the chalcogenide layers are trigonally coordinated with three atoms per unit cell. Finally, the tc-TMDs have a unit cell which contains 12 atoms, with a single layer of metal atoms sandwiched between the chalcogen atoms, which are buckled as shown in Fig. 1(c). The buckling along both of the in-plane directions has physical implications for the tc-TMDs, as many of their tensorial properties are asymmetric.

Before determining the physical properties of these materials, we first examine the influence of the choice of the pseudopotentials, the treatment of relativistic effects (spin-orbit coupling), and of the approximation of the long-range $e^- - e^-$ correlation on the proper description of the TMDs.

### A. Choice of pseudopotentials

We investigate the effects of different pseudopotential approximations on the DFT and DFPT calculation by comparing the OPIUM [47], FHI98PP [48], and ONCVPSP [49,50] generation codes, and find that there are negligible effects on the DFPT calculation for “well-built” pseudopotentials [51,52]. The hardest cases are the CDW compounds TiS$_2$ [21], TiSe$_2$ [19,20], NbS$_2$ [16,17], and NbSe$_2$ [13,14], whose specific instabilities are very sensitive to volume and pseudopotential, though their qualitative physics is correct in each case. We do not focus on the CDW aspect or enter into the debates on its nature and details. For completeness and comparison to others, we thus include both the Nb- and Ti-based CDW TMDs, although we actually treat these materials using their average, translationally invariant geometry.

The only unsatisfactory pseudopotentials were those generated with the FHI98PP code [53] for elements W and Ti [54]. Therefore, unless specifically mentioned, our results use GGA-PBE (Perdew-Burke-Ernzerhof) pseudopotentials, generated with the FHI98PP code (which are slightly softer), for all atoms except W and Ti. We use a norm-conserving pseudopotential generated with the OPIUM code for W and one generated with the ONCVPSP code for Ti.

### B. Effect of spin-orbit coupling

It has been shown that the spin-orbit interaction (SOI) can make a significant correction to the phonon band structure of certain systems [55–57], particularly at the zone edge. To investigate the effects of the inclusion of SOI on the phonon band structure, we calculated the phonon band structure using ONCVSP pseudopotentials [49], with and without the spin-orbit projectors (see Ref. [51] for the SOI method) for both atomic species in several compounds, among them MoTe$_2$ and ReSe$_2$. The result of this calculation is shown in Fig. S1 of the SM [34] for MoTe$_2$, the heaviest of the compounds per formula unit.
investigated here, and ReSe₂, the compound with the largest atomic number. In Fig. S1 of the SM [34] the phonon band structures are shown without the spin-orbit projectors in black and with the spin-orbit projectors in red. The inclusion of the SOI made little difference in the lattice parameters, provided a small spin splitting of the valence bands, and had a negligible effect on the phonon band structure of the TMDs, especially the lattice modes when compared to the effect of including the dispersion corrections. Due to the correlation between the changes in the electronic and phonon band structures, our calculations show that the SOI modifies the phonon band structure through the electronic band structure and does not have a direct effect on the calculated interatomic force constants.

C. Effect of the long-range $e^-e^-$ correlation approximation

While a precise description of layered semiconductor materials requires a more advanced description of the long-range electron-electron correlation (see Refs. [58,59]), DFT in its usual approximations—LDA and GGA—is sufficient to properly describe the vibrational properties of most ionic, metallic, or covalent compounds. With this in mind, our calculations of the bulk TMDs use three different dispersion schemes given by Grimme [30–32], which are known to have a strong effect [60,61] on electronic and vibrational properties. These dispersion schemes, known as DFT-D, are based on simple atomic pairwise terms, with environmental-dependent dispersion coefficients tabulated beforehand using time-dependent DFT that do not have the computational overhead of other vdW implementations [62–70]. The result of this calculation for the lattice parameters is shown in the SM [34]. This calculation and others on the vibrational properties indicate that the DFT-D3 scheme provides the most accurate lattice parameters when compared to measurement. More generally, the performance of the most-popular vdW functional and dispersion schemes have been assessed recently [71], and DFT-D3 is performing relatively well compared to more elaborate methods. Thus, for all the following calculations, the DFT-D3 scheme is used as part of our DFT and DFPT calculations.

The dispersion corrections influence the phonon frequencies in two different ways: first, through geometric changes when compared to calculations with no dispersion corrections, as highlighted in Table S1 of the SM [34], and second, through their direct contribution to the interatomic force constants as derived in Ref. [60]. The former is generally assumed to be important, as was shown in Ref. [72]. The latter is generally assumed to be negligible due to the small contribution of dispersion corrections to the total energy (10–100 meV/atom); however, we show here that the dispersion corrections cannot be neglected in the case of TMDs. Still, disentangling the effects of the geometry modification and of the direct contributions to the interatomic force constants needs careful consideration.

To do so, the influence of geometry modification on the phonon frequencies is first estimated using the Grüneisen parameter [73], defined as

$$\gamma_i(q) = -\frac{\partial \ln(\omega_i(q))}{\partial \ln V},$$

where $V$ is the volume of the unit cell and $\omega_i(q)$ is the phonon frequency of the $i$th mode at momentum $q$. The result of this finite-difference calculation using three different volumes which deviate from the fully relaxed volumes by

![FIG. 3. (a) Raman spectra for MoTe₂ with three different polarizations corresponding to a DFT-D3/DFT-D3 calculation in which the Raman signals relate to our calculation (in black) of the $\Gamma$ point phonons in (b). (b) Calculated phonon band structure of MoTe₂ along a path of high-symmetry points in $q$ space. The red lines correspond to a DFT-D3/DFT calculation, and the black lines correspond to a DFT-D3/DFT-D3 calculation in which the DFT-D3 scheme is used during both the DFT and DFPT calculation. (c) Phonon density of states corresponding to the same color scheme as in (b). Experimental data points correspond to the measurements in Ref. [46]. The high-symmetry path comes from Ref. [33].](image-url)
TABLE I. Calculated properties of bulk MoS$_2$, ZrS$_2$, and ReS$_2$. Our calculations are given as the first column, experimental measurement as the second column, and the reference to the experimental work in the third column for each material. We report the in-plane lattice parameters $a$ and $b$, the out-of-plane lattice parameter $c$, the components of the elastic tensor $c_{ij}$, Young’s modulus $E$, Poisson’s ratio $\nu$, bulk modulus $B$, electronic band-gap energy $E_g$, components of the static dielectric tensor $\epsilon^{\infty}_{ij}$ and the optical dielectric tensor $\epsilon^{\infty}_{ij}$, components of the Born effective charge tensor on the transition metal atom $Z_{ii}$, Debye temperature $\theta_D$, average sound velocity $v_{\text{avg}}$, and the zero-temperature phonon free-energy $\Delta F(0)$. The local environment of the tc-TMDs gives rise to two values of each component of the Born effective charge.

|                | MoS$_2$    | ZrS$_2$    | ReS$_2$    |
|----------------|------------|------------|------------|
|                | Calc.      | Exp.       | Calc.      | Exp.       | Calc.      | Exp.       |
| $a$ (Å)        | 3.162      | 3.160 [76] | 3.687      | 3.660 [77] | 6.420      | 6.362 [78] |
| $b$ (Å)        | 6.587      | 6.465 [78] |            |            | 1.999      | 1.55 [81]  |
| $c$ (Å)        | 12.301     | 12.290 [76]| 5.812      | 5.850 [77] | 6.999      | 6.401 [78] |
| $E_g$ (eV)     | 0.886      | 1.23 [79]  | 1.041      | 1.68 [80]  | 1.199      | 1.55 [81]  |
| $c_{11}$ (GPa) | 210.77     | 238 [82]   | 122.00     | 227.06     |            |            |
| $c_{22}$ (GPa) | 249.80     |            | 122.00     | 227.06     |            |            |
| $c_{33}$ (GPa) | 44.41      | 52 [82]    | 6.71       | 82.81      |            |            |
| $c_{44}$ (GPa) | 17.15      | 19 [82]    | 11.07      | 27.02      |            |            |
| $c_{55}$ (GPa) | 6.71       |            | 6.71       | 6.39       |            |            |
| $c_{66}$ (GPa) | 81.17      | 91 [82]    | 48.92      | 82.81      |            |            |
| $E_x$ (GPa)    | 198.65     | 240 [83]   | 115.68     | 196.41     |            |            |
| $E_y$ (GPa)    | 211.76     |            | 115.68     | 196.41     |            |            |
| $E_z$ (GPa)    | 43.84      | 32.74      | 25.54      | 25.54      |            |            |
| $\nu_{xy}$    | 0.22       | 0.27 [83]  | 0.19       | 0.18       |            |            |
| $\nu_{xz}$    | 0.03       | 0.05       | 0.04       | 0.04       |            |            |
| $\nu_{yz}$    | 0.03       | 0.05       | 0.04       | 0.04       |            |            |
| $B$ (GPa)      | 66.35      | 53.40 [84] | 39.90      | 71.14      |            |            |
| $\epsilon_{xx}$| 15.53      | 15.4 [85]  | 37.23      | 16.21      |            |            |
| $\epsilon_{yy}$| 6.87       | 6.28 [85]  | 10.20      | 5.81       |            |            |
| $\epsilon_{zz}$| 15.31      | 15.2 [85]  | 9.94       | 15.75      |            |            |
| $\epsilon_{12}$| 6.82       | 6.25 [85]  | 5.54       | 7.23       |            |            |
| $\epsilon_{13}$| 14.14      |            | 14.14      | 7.23       |            |            |
| $\epsilon_{23}$| 14.14      |            | 14.14      | 7.23       |            |            |
| $Z_{xx}^*$ (e) | -1.09      | [1.1] [85] | 6.19       | 15.75      |            |            |
| $Z_{yy}^*$ (e) | -0.79      |            | -0.79      | 7.23       |            |            |
| $Z_{zz}^*$ (e) | -0.34      |            | -0.34      | 7.23       |            |            |
| $\theta_D$ (K) | 262.64     | 260 [88]   | 290.87     | 147.07     | 115 [89]  |            |
| $v_{\text{avg}}$ (km/s) | 4.181 | 3.996 | 3.000 | 48.09 |            |            |
| $\Delta F(0)$ (kJ/mol) | 30.45 | 10.96 |            |            |            |            |
Fig. 4. (a)–(f) A comparison between our DFT and experiments for some of the principal vibrational and dielectric properties. Symbols (colors) represent different symmetry classes: h-TMDs (black), t-TMDs (blue), and tc-TMDs (red). (a) In-plane lattice parameter, (b) out-of-plane lattice parameter, (c) indirect energy gap, (d) static dielectric constant, (e) absolute value of the in-plane Born effective charge on the transition metal atom, and (f) Debye temperature. Points correspond to cases where both calculated and experimental data were found. The light-gray wedge represents an error of ±5%. The overall agreement is very good, but the electronic gap is quite scattered, for reasons described in the text, whereas the dielectric constant is well reproduced. In (g)–(l) we show trends in our calculated data with respect to the atomic number of the transition metal or atomic mass per formula unit (f.u.). Lines are linear fits to the available data. For comparison, we plot half the out-of-plane lattice parameter for the hexagonal compounds in (b) and (h), and in (a) and (g) we plot half the in-plane lattice parameter for the triclinic compounds.

computed with and without dispersion corrections for MoTe$_2$ are represented in Fig. 3. In the Raman spectra shown in Fig. 3(a), the dispersion corrections, and their effects on the electronic and structural properties, are included in both parts of the calculation (DFT and DFPT), since these quantities are related to the derivatives of energy with respect to the electric field, and, as the DFT-D3 correction is independent of the electron density, there are no additional terms in the third-order derivatives due to the dispersion correction [60,75]. As one can see, the dispersion corrections have a drastic influence on the phonon band structure, not only on the intralayer modes but for interlayer modes as well.

Having considered the effects of the normal approximations used in first-principles calculations, and shown which is the most important, we now outline our calculations of the physical properties of the TMDs. For all the calculations found below and in the SM [34], we use the pseudopotentials mentioned previously, no spin-orbit interaction, and the DFT-D3 dispersion scheme.

III. STRUCTURAL AND ELECTROMECHANICAL PROPERTIES

The physical properties of the system, namely, the lattice constants, elastic properties, and piezoelectric properties, are determined as part of our DFT and DFPT calculation. In particular, our calculations of the relaxed lattice parameters, shown in Table I and the SM [34], show good agreement with experimental measurement [16,76–78,82–84,90–99]. Indeed, we find that as the atomic number of the transition metal increases for each family of compounds, the out-of-plane lattice constants increase in a near linear fashion. A comparison of our calculated lattice parameters with respect to experimental measurement is given in Figs. 4(a) and 4(b) for the in-plane and out-of-plane lattice parameters with the relationship to the transition metal (TM) atomic number given in Figs. 4(g) and 4(h). The result of this analysis shows that, for the h-TMDs, our calculated lattice parameters lie within 0.7% and 2.0% for the in-plane and out-of-plane lattice parameters, respectively. In the case of the t-TMDs, our calculations are within 2.2% for
both sets of lattice parameters. Similarly, for the tc-TMDs, our calculations lie within 2.0% for the in-plane and out-of-plane lattice parameters (except for the c lattice parameter of ReSe$_2$). The rescaling of the c lattice parameter due to the dispersion corrections, as shown in Table S1 of the SM [34], shows clearly why the dispersion corrections are important for accurate calculations of layered materials.

Our DFPT calculations allow us to determine several elastic properties which are easily compared to experiment. Since the elastic tensor displays the underlying symmetry of the lattice, there are five unique elastic constants for the h and t compounds and 21 unique elastic constants for the tc compounds. Our data tables provide the principal components of the elastic tensor for each of the compounds and the derived elastic properties, such as the bulk modulus, whose relationship to the elastic tensor is outlined in the SM [34]. These materials are well known for their use as lubricants, and we find that the elastic coefficient responsible for the sliding between layers, c$_{44}$, is small in these materials, comparable to graphite (c$_{44} = 4.25$ GPa [100]), and that the magnitude of the bulk modulus, $B_c$, generally decreases as the mass of the formula unit increases, as shown in Fig. 4(j).

Likewise, we find a general overestimation of the bulk modulus when compared to experimental values, contrary to early work by Filippi et al. [101] who found a general underestimation using GGA exchange correlation. This discrepancy between our calculations and those of Filippi et al. is likely caused by our stricter convergence parameters and different pseudopotentials, possibly the cause of our better agreement with the experimental lattice constants, propagating then to different elastic properties. For the symmetry classes considered here the piezoelectric tensor components are identically zero due to the presence of mirror plane symmetry [102,103].

IV. ELECTRICAL, DIELECTRIC, AND OPTICAL PROPERTIES

The electrical, dielectric, and optical properties of the system are central to the most promising applications of the TMDs. Using DFT and DFPT, for the semiconducting systems, we calculate the band-gap energy, dielectric tensors, Born effective charge tensor, nonlinear optical tensor, and Raman susceptibility. For the symmetry classes considered here, the nonlinear optical tensor components are identically zero due to the presence of mirror plane symmetry [102,103]. These calculated properties are shown in Table I and in the SM [34], where we also provide the indirect band-gap energy and compare to experimental data [77,79,81,85–87,89,104–112].

Our calculation of the indirect energy gap comes from the Kohn-Sham electronic band structure of these materials as shown in Fig. 5 for our three example compounds. Here, the band structures are plotted along a path in $k$ space determined by the underlying symmetry of the system. In each case, the zero of energy is set to the Fermi level or to the top of the valence band. With the exceptions of the metallic compounds [16,77], these materials all have an indirect band gap originating at $\Gamma$ and ending along the path from M to K. Most of the calculated gap energies are smaller than their experimentally measured counterparts [see Fig. 4(c)]. This is due to a fortuitous cancellation of errors between the usual DFT Kohn-Sham noticeable underestimation of the quasiparticle band gap and the large exciton binding energy (the difference between the quasiparticle and optical band gap). Indeed, due to long-range electrostatics in these layered materials, the exciton binding energy, which determines the optical gap, is very large and compensates the DFT underestimation of the real quasiparticle gap [113–115]. This effect is even stronger in monolayers [116–119]. Compared to calculations without any treatment of the long-range $e^- - e^-$ correlation, our calculations with GGA and vdW dispersion corrections are more consistent with experiment. Given the limitations of the calculated band structure, our calculations of the zero-frequency dielectric constant compare well to experiment, as shown in Fig. 4(d), with much less spread in the data, meaning that the static dielectric constant, calculated as part of our DFPT calculation using the methods outlined in Ref. [36], is well represented due, in part, to the fortuitous cancellation of errors.

The Born effective charges, which give the dynamic response of the system to a displacement and electric field perturbation of the system, display signs which are counterintuitive, i.e., the transition metal takes the negative charge for the h and tc compounds. A discussion of the Born effective charge tensor and the origin of the counterintuitive charge is found in Ref. [120]. To compare to the measured value of the Born effective charge requires care, as only the absolute value of the Born effective charge is easily accessible experimentally. Therefore, experimental values of the effective charge are given in terms of an absolute value and are compared to our
V. PHONON BAND STRUCTURES, THE DENSITY OF STATES, AND RAMAN SPECTRA

The thermal and acoustic properties of our compounds come from a calculation of the phonon dispersions. From this calculation, the Helmholtz free energy $\Delta F$, entropy $S$, and constant-volume specific heat $C_v$, are determined as a function of temperature using the phonon density of states $g(\omega)$, as laid out in Ref. [121]. A plot of these quantities is shown in Fig. S9 of the SM [34]. The Helmholtz free energy at $T = 0$ K is given in the data tables and shown in Fig. 4(i), which shows a decrease as the atomic mass of the formula unit increases. Our calculations of the Debye temperature and average sound velocity come from summing up the Debye temperature and average sound velocity at each $q$ point (in reduced coordinates) such that $|q| < 0.25$ and then dividing by the number of points within that radius, which is determined by the density of our $q$-point mesh ($30 \times 30 \times 30$). This Debye temperature agrees reasonably well with experiment, as shown in Fig. 4(f) [88,89,122–124]. Similar to the free energy, the Debye temperature decreases with the increasing atomic mass of the formula unit.

In addition to the electronic band structure, our calculations of the phonon band structures, phonon density of states, and Raman spectra allow us to determine the quality of our calculations by comparing to neutron scattering and Raman and infrared experimental measurements. In Fig. 6 and the figures in the SM [34], the calculated phonon band structures, atom-projected phonon density of states, and Raman spectra for the three example compounds are shown and compared to experimental data for the Raman-active and infrared-active modes at $\Gamma$ and neutron scattering data at finite $q$. In particular, neutron scattering data [93,98,125,126] and Raman and infrared measurements [45,46,127–137] are used to compare to our calculations.

In Fig. 6, all the Raman spectra in the SM [34] are shown with the atom-projected phonon density of states for the transition metal atoms (in blue) and chalcogen atoms (in red). Our calculations of the phonon band structure, density of states, and Raman spectra for the Ti-based compounds show indications of charge-density waves or Kohn anomalies.
and, in agreement with recent experimental work, we find no charge-density wave in bulk TlTe₂ [142]. The phonon band structures of the Nb-based compounds, also shown in the SM [34], reveal several unstable modes due to the metallic nature of the compounds and the limitations of the harmonic approximation when determining the phonon band structure in these materials [143].

We give the numerical values of our calculated Raman- and infrared-active modes in Table S2 of the SM [34] for the h-TMDs to show that our calculations for these modes are within 3.0% of the experimental measurements. Here the identified phonon modes are in accordance with the Bilbao crystallographic server [144–146]. As an additional check of the effect of the dispersion corrections on the phonon frequencies, we show in Table S2 of the SM [34] the Raman- and infrared-active modes using both DFT-D3 and DFT-D3(BJ) for the dispersion corrections. These two methods differ in how they treat interactions at short distances, i.e., as $R \to 0$ [31,32]. From this calculation, we find that using DFT-D3 results in a better agreement with experimental measurements for the low-energy phonon branches.

VI. CONCLUSIONS

The various approximations used in DFT and DFPT, namely, the pseudopotential, spin-orbit, and van der Waals interaction, are often used when investigating the properties of layered materials. These approximations are important to consider when undertaking calculations of layered materials, as they can have a large impact on the structural and vibrational properties of the system. Here, it was found that the physical properties of the system depend strongly on the van der Waals approximation and to a lesser extent on the spin-orbit approximation. Therefore, our calculations included the van der Waals interaction in our DFT and DFPT calculations, which gives rise to good agreement between our values of the vibrational and dielectric properties when compared to experiment, as shown in Fig. 4. Thus our predicted values for the unmeasured quantities are believed to be accurate and useful for future comparison to experimental measurements.

Surprisingly, despite the well-known shortcomings of density functional theory in the GGA approximation, yielding an inaccurate calculation of the electronic band-gap energy, we are still able to accurately calculate the dielectric properties of this material. Additionally, comparisons with and without the dispersion corrections in the DFPT calculation led to the conclusion that the corresponding additional contributions during the DFPT calculation are critical to the accuracy of the calculated vibrational properties.

In conclusion, our careful testing of the various approximations normally used in DFT and DFPT calculations indicate that care must be taken when calculating the vibrational and dielectric properties of the transition metal dichalcogenides. Our calculations of the mechanical, electrical, optical, thermal, and acoustic properties of a subset of the transition metal dichalcogenides used the ABINIT software package, the van der Waals scheme known as DFT-D3, and norm-conserving pseudopotentials. Due to the sensitivity of the vibrational properties on the lattice parameters and interatomic force constants, we use dispersion corrections during our DFT and DFPT calculations for all of the transition metal dichalcogenides and provide experimentally relevant results within our data tables for many unmeasured quantities. It is our hope that this data is used as part of a much larger effort to engineer heterostructures which combine the unique properties of each individual material.

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