Electroweak Baryogenesis from Late Neutrino Masses

Lawrence J. Hall,1,2 Hitoshi Murayama,1,2 and Gilad Perez1

1Theoretical Physics Group, Ernest Orlando Lawrence Berkeley National Laboratory, Berkeley, CA 94720
2Department of Physics, University of California, Berkeley, CA 94720

Electroweak Baryogenesis, given a first order phase transition, does not work in the standard model because the quark Yukawa matrices are too hierarchical. On the other hand, the neutrino mass matrix is apparently not hierarchical. In models with neutrino mass generation at low scales, the neutrino Yukawa couplings lead to large CP-violation in the reflection probability of heavy leptons by the expanding Higgs bubble wall, and can generate the observed baryon asymmetry of the universe. The mechanism predicts new vector-like leptons below the TeV scale and sizable $\mu \rightarrow e$ processes.

The neutrino physics has been undergoing a revolutionary progress in the past several years. The recent observations of neutrino mass conversion in solar, atmospheric and reactor neutrino experiments provided firm evidence for physics beyond the Standard Model (SM) (see e.g. [1, 2] and refs. therein). The new data on the distance/energy-dependence of atmospheric neutrinos [3] and the recent spectrum analysis from the reactor experiments [4] indicate oscillatory behaviour. This strongly favors the presence of tiny but non-zero neutrino masses.

The most popular explanation for the origin of neutrino masses is the seesaw mechanism [5]. In its minimal form, right-handed neutrinos are introduced with lepton-number violating Majorana mass terms, $\Delta_L^T N N$, as well as Yukawa couplings to the SM lepton doublets $l$ and the Higgs $h$, $Y_L h N l$. The oscillation data requires $\Delta_L \sim 10^{14}$ GeV if $Y_L \sim O(1)$. Moreover, the seesaw mechanism naturally provides a way to account for the observed baryon asymmetry of the universe (BAU) [1, 2], $n_B/s \sim 8 \times 10^{-11}$, where $n_B/s$ is the baryon to entropy ratio. The out-of-equilibrium decay of the right-handed neutrinos creates a lepton asymmetry, which is partially converted to a baryon asymmetry by the electroweak sphaleron process (leptogenesis) [6]. Thermal leptogenesis typically requires, however, $\Delta_L \sim 10^9$ GeV [8] with somewhat small Yukawa couplings $Y_L$ and large hierarchies in the right-handed masses.

While the seesaw mechanism is very appealing theoretically, it is unlikely that it will be subject to a direct experimental test in the near future. It is important to explore other possibilities for the origin of neutrino masses. One such example is the late neutrino mass framework that induces small neutrino mass due to a low scale of symmetry breaking [9]. When this symmetry is broken, say by a set of symmetry breaking VEVs, $\langle \phi \rangle = f$, the neutrinos acquire masses from operators

$$ \left( \frac{\phi}{M_F} \right)^n 1 N h \quad (\text{Dirac}) \quad \text{or} \quad \left( \frac{\phi}{M_F} \right)^n (h h)^2 \quad (\text{Majorana}), $$

(1)

We stress that this does not depend on the details of the model, or whether one uses global [10] or gauge [11, 12, 13] symmetries. The strongest limits on $f$ arise from big bang nucleosynthesis [14, 15, 16, 17, 18] and from observation of supernova neutrinos [19]: for $n = 1$, $f \gtrsim 10$ keV, while more powerful limits apply to higher $n$. It is remarkable that new physics at such a low scale is not excluded by direct experimental data.

In this letter we show that the late neutrino mass framework can naturally realize leptogenesis at the electroweak (EW) phase transition [14]. Heavy vector-like leptons that give rise to the operators [10] bounce off the expanding bubble walls with $O(1)$ Yukawa couplings, and acquire a large asymmetry. They quickly decay to the standard-model leptons and the sphaleron process partially converts their asymmetry to the baryon asymmetry. Thus our mechanism leads to various predictions that can be tested by near future experiments. Here we focus on the qualitative features of our scenario while a more detailed analysis will be presented in a following publication. We simply assume that the phase transition is first order, and focus on the size of the baryon asymmetry as well as phenomenological constraints on the model. We briefly comment on the origin of the first-order phase transition towards the end of this paper.

The Model and Mechanism. As well as introducing a low scale $f$, theories of late neutrino masses introduce flavor scales that are much lower than the scale $\Delta_L$ of the seesaw mechanism. One economical possibility, that we explore in this letter, is that these flavor scales are all of order the EW scale: $M_F, \Delta_L \sim v \equiv \langle h \rangle$. In this case the non-SM states that generate the operators of (1) have masses of order $v$ and are available to take part in EW baryogenesis. The flavor symmetry breaking scale becomes $f \sim v (m_N/v)^{1/n} \sim (m_N, 100 \text{ keV}, 30 \text{ MeV}...) \text{ for } n = 1, 2, 3...$ The $n = 1$ case is excluded by BBN and supernova constraints. Large $n$ theories may be preferred in the sense that the scale $f$ grows and requires less protection. In this letter, we describe a simple $n = 2$ theory that illustrates our baryogenesis mechanism.

We focus on the Majorana case since, as shown below, the Dirac case is disfavored by the direct experimental data for the parameter range that produce enough baryon asymmetry.

The minimal model for late Majorana neutrino masses is

$$ \mathcal{L}_\nu = Y h N L + M L^c L + y \phi L^c l + \frac{M_N}{2} N N + h.c., \quad (2) $$

where $L, L^c$ are vector-like lepton doublets, and the couplings $Y, y$, and the masses $M, M_N$ are $3 \times 3$ flavor matrices. We consider all eigenvalues of $M$ to be comparable, the same for $M_N$, and those of $Y$ to be of $O(1)$. This is suggested by the lack of hierarchy (anarchy [17]) in the neutrino masses. We
refer to their eigenvalues as $\tilde{M}, \tilde{M}_N$, and $\tilde{Y}$. There may be a moderate hierarchy in the eigenvalues of $y_i$. Note that there is a lepton analogue of the rephasing invariant Jarlskog determinant even for just two generations ($N_G = 2$) \cite{(22)}.

$$J_L = 3m_{\nu} \text{Tr} \left(YY^\dagger M_N^2 \bar{Y}^* Y^T M_N M_N^T M_N \right). \quad (3)$$

Below the scales $\tilde{M}$ and $\tilde{M}_N$, neutrino masses are described by the operator $(y_i^2 Y_i^2/M^2 M_N)^2 h^2 \phi^2$, corresponding to the $n = 2$ case of \cite{(3)}, so that the flavor symmetry breaking scale is predicted to be

$$f^2 \sim \frac{m_{\nu} v}{y_i^2 Y_i^2} \frac{\tilde{M}^2 \tilde{M}_N}{v^2} \frac{(100 \text{keV})^2}{y_i^2 Y_i^2} \frac{\tilde{M}^2 \tilde{M}_N}{v^2}. \quad (4)$$

A low $f \sim 100$ keV would imply that the $\phi$ states contribute to the energy density of the universe during BBN. However, our baryogenesis mechanism will require $\tilde{M}, \tilde{M}_N$ somewhat larger than $v$, and lepton flavor violation will constrain $y_i$ to be somewhat small. Hence we expect that the $\phi$ states are heavier than 1 MeV and decay to neutrinos before BBN.

Let us now describe our main mechanism. With $\tilde{M} \sim v$, during the electroweak phase transition $L$ particles and their CP conjugates, $\bar{L}$, are reflected differently from the Higgs bubble wall. This is due to the presence of unsuppressed CP violating phases in $Y, M,$ and $M_N$ (for a related idea see \cite{(13) (19)}). Thus an asymmetry in $L$ is induced in the region just in front of the wall. As shown below, the size of this asymmetry is expected to be of order $J_L/\tilde{M}_N^4$. We assume the $L \to Nh$ decay process is kinematically forbidden (i.e., $\tilde{M}_N > \tilde{M}$) so that the asymmetry is transferred to SM leptons via $L \to l\phi$ decays. The presence of the asymmetry in the SM lepton doublets biases the sphaleron rate to induce a B production in the vicinity of the wall. When the expanding bubble passes over this region, the sphaleron processes decouple, freezing in a B asymmetry. Outside the bubble the sphaleron rate $\Gamma_{SP} \sim \alpha_i Y_i T_e, T_e$ being the critical temperature, is much slower than other dynamical scale near the bubble wall \cite{(20)}. Thus the baryon asymmetry could be as large as

$$\frac{n_B}{s} \sim \frac{1}{g_\ast} \frac{\alpha_i^4 \Gamma_{SP}}{\tilde{M}_N^4} \sim 10^{-8} \quad (5)$$

where $g_\ast \sim 100$ is the number of relativistic degrees of freedom, and anarchical neutrino masses suggest that $J_L/\tilde{M}_N^4$ is of order unity. Below we study what other factors might suppress the baryon asymmetry.

**Estimating the Baryon Asymmetry.** To have a semi-quantitative estimation of the resultant BAU, we apply the thin wall approximation (the validity of this approximation depends on the details of the mechanism which produces the 1st order phase transition \cite{(20)}). We first estimate the density difference between $L$ and $\bar{L}$, $n_L$, induced by the reflection asymmetry \cite{(21)}

$$\frac{n_L}{s} \sim \frac{1}{45 T_c^2} \int \frac{d\omega}{2\pi} n_0(\omega) [1 - n_0(\omega)] \Delta(\omega) \Delta p^2 \cdot \bar{v}_w, \quad (6)$$

where $v_w \sim 0.1$ is the wall velocity and $n_0(\omega) = 1/(e^{\omega/T_c} + 1)$ is the Fermi-Dirac distribution. The difference between $N$ and $L$ momenta for a given energy, $\Delta \bar{p} \equiv \bar{p}_L - \bar{p}_N$, is large, due to $O(1)$ mass differences among $\tilde{M}$ and $\tilde{M}_N$. This is welcome because, in the SM, $\Delta p$ arises only due to the electroweak thermal corrections to the masses, and is suppressed by $\alpha_W$ \cite{(21)}. The reflection asymmetry $\Delta(\omega)$ is given by \cite{(20)}

$$\Delta(\omega) = \text{Tr} \left( R_{NL}^2 R_{NL} - R_{NL}^2 [R_{NL} R_{NL}] \right),$$

where $R_{NL}$ is the reflection coefficient for $N \to L$ and the bars stand for the CP conjugated process.

In order to calculate the reflection asymmetry from the bubble wall, we have computed the Green function for our model in the simplifying limit $\tilde{M}_N \gg \tilde{M}$. Using a perturbative expansion in $Yv/T_e, M/\omega$, and for $N_G = 2$, we find $\Delta(\omega) \sim \left( \frac{\varepsilon v/T_e}{M} \right)^{2N_G} J_L$ where $\varepsilon \sim 10/T$ is the mean free path for the leptons \cite{(21)} (see Fig. 1). Below we find that phenomenological constraints favor somewhat heavier RH Majorana masses, $\tilde{M}_N \gtrsim 10v$. In this case a suppression in the reflection asymmetry is expected since the heavy incoming particle is hardly affected by the potential barrier. This effect cannot be captured using an expansion in $M_N/\omega$. We estimated the corresponding $1/M_N$ suppression by analysing a single generation reflection problem which can be solved analytically. We indeed found that the reflection amplitude is further suppressed via $(\tilde{Y}/M_N)^{2N_G}$. Consequently, in the relevant region of parameter space the reflection asymmetry is given by

$$\Delta(\omega) \sim \left( \frac{\varepsilon v/T_e}{M} \right)^{2N_G} \text{Tr} \left( \frac{\varepsilon v/T_e}{M} \right)^{2N_G} J_L \theta(\omega - M_N). \quad (7)$$

where $J_L$ is even in the case of interest where $Yv/T_e$ and $M/\omega$ are of order unity.

Below we use the estimate \cite{(7)} even in the case of interest where $Yv/T_e$ and $M/\omega$ are of order unity.

The rate for baryon production is approximately $dn_B/dt \sim 3T_c^2 \Gamma_{SP} \Delta F/2 \Delta F$. $\Delta F$ is the free energy difference between two neighboring zero field-strength configurations, for which $\Delta B = \Delta L = 3$ (provided that $\Gamma(L \rightarrow l\phi)$ is not much slower than other thermalization rates; see below). $\Delta F$ is calculated in the presence of a hypercharge density $n_Y \sim -n_L/2 \Delta F$. (More correctly, one should define a global approximately conserved charge orthogonal to hypercharge $B' = B - xY$ where in our case $x = 1/7$ \cite{(22)}. We verified that

![FIG. 1: Perturbative calculation of the reflection coefficients which picks up the Jarlskog invariant $J_L = 3m_{\nu} \text{Tr}[(YY^T)^2 M_N^2 M_N^T M_N]$ from the one-particle cuts in the amplitudes.](image-url)
this will hardly modify our results). In our case we find that\[ \Delta F \approx n_L/T_c^2. \]The BAU is obtained by integrating \( dnB/dt \), which we estimate via \( nB \sim \int nB/dt \times \ell_w/\nu_w \) where \( \ell_w \) is the typical penetration length for the non-zero global charge which flows through the plasma in the unbroken phase. With fast massless leptons one expects, from estimation of energy loss in the plasma \([23]\), \( T_c \ell_w = O(100) \) \([21, 22]\). In our case, with semi-relativistic leptons, the penetration distance is shorter even though the energy loss rate is very low, because the massive leptons rather quickly lose their directionality (away from the wall). For instance, elastic scattering of a lepton of mass \( 4T_c \) with a plasmon that carries a perpendicular momenta, \( T_c \), roughly results in 25% momentum loss in the original direction of motion for the lepton. Thus in our case we estimate \( \ell_w \sim N_{\text{coll}} \ell_T \) where \( N_{\text{coll}} \) is the average number of collisions that a lepton undergoes before its directionality is lost. Below, we assume \( N_{\text{coll}} = 2 \).

Using Eqs. (3)\( ^6 \) we obtain
\[
\frac{nB}{s} \sim 3 \Gamma_{\text{Sp}} N_{\text{coll}} \ell_T/n_L \nu_w 2 s. \tag{8}
\]

Our next step is to identify the dependence of the resultant BAU on the model fundamental parameters. Assuming that CP violation is maximal and taking for simplicity \( (\bar{Y} v)^2 \ell_T/T_c \sim 1 \) we find \( \Delta(\omega) = (T_c/\omega)^4 \theta(\omega - M_N) \). In addition, fixing \( N_{\text{coll}} = 2 \) and \( \ell_T \sim 10/T_c \) we can numerically compute the resultant BAU as a function of \( M_N/T_c \). As \( M_N/T_c \) increases, the BAU rapidly decreases due to both a Boltzmann suppression factor [see Eq. (3)] and also a polynomial one \( (7) \). In fig. 2 we plot \( nB/s \) as a function of \( M/T_c \). We find that the observed asymmetry can be accounted for when \( M_N \lesssim 4 \times T_c. \tag{9} \)

In the Dirac case \( N_{\text{col}} = 3 \) and the resultant asymmetry is further suppressed.

**Direct Constraints and Tests.** In the following we briefly discuss the direct phenomenological constraints on our scenario and discuss several ways to directly test our model in the near future.

**Electroweak precision measurements.** Our model requires additional fields, namely heavy lepton doublets charged under the SM gauge group. Because they are vector-like, the \( S \) parameter is hardly affected. The Yukawa couplings to the SM Higgs, \( Y^\ell \), breaks the custodial isospin symmetry and therefore modify the \( T \) parameter. The additional contribution to the \( T \) parameter from the three vector-like lepton doublets, \( T_L \), is similar to a single extra vector-like top quark \([23]\) \( T_L \sim T_{\text{SM}}^0 Y^\ell \frac{\nu}{m_t^2} \) where \( T_{\text{SM}}^0 \sim 1.2 \) is the SM-top contribution to \( T \) \([1]\) and \( m_t \) is the top mass. Requiring the \( T_L \lesssim 0.2 \) we find the following lower bound
\[
M \gtrsim 2.5 \times \bar{Y} \left( \frac{Y \nu}{m_t} \right). \tag{10}
\]

Furthermore, in the Dirac case, the light RH neutrinos are a linear combination of \( N \) and \( L' \), and hence the \( Z \) can decay invisibly to these states. The rate is proportional to the quartic power of the corresponding mixing, \( M/T_c \). Using the 3σ range (to allow for at least three neutrinos) \([23]\) we find that 3.01 neutrinos are allowed. For three extra generations this implies \( M \gtrsim 4 \times \bar{Y} \nu \). (This constraint is absent in the Majorana case.)

**Lepton flavor violation.** The Yukawa couplings to the SM leptons, \( y^\ell \), are generically not aligned with \( M, M_N \) and \( Y \) and hence induce lepton flavor violation. This will contribute to processes such as \( \mu \to e \) conversion which are highly constrained by experimental data \([1, 26]\). In our model the SM leptons couple to the additional fields only through \( y \), the Yukawa coupling to \( \phi \). To avoid these constraints naturally, a mild hierarchical structure is required for \( y \). For example, in the appropriate basis, \( y \sim \text{diag} (10^{-2}, 10^{-1}, 10^{-1}) \), which is consistent with the neutrino flavor parameters \([27]\) provided that \( M_N, M, Y \) are anarchical. The smaller the eigenvalues of \( y \), however, the smaller is the decay rate \( \mu \to \tau \phi \). Comparing the decay rate into SM doublets to the thermalization time scale we find \( \Gamma_{\mu \to e} \nu_w \sim 10 y^2 \frac{M}{T_c} \sim 0.25 - 1 \) which implies further suppression in the resultant BAU (this, given our crude estimation see fig. 3, is still consistent with the observed value). We thus find that there is a tension between producing sizable BAU and suppressing the contribution to lepton flavor violation.

**Collider physics.** From Eqs. (9)\( ^9 \), our scenario predicts the presence of SU(2) doublets with masses below the \( O(1 \text{ TeV}) \) range. These contain charged particles, with masses above 100 GeV from current bounds \([4]\), that may be produced and detected at the LHC, or better at the ILC. A clear signal at the LHC is expected if the vector-like leptons are sufficiently light, via production of \( L^+ L^- \) which decay to a single, energetic SM charged lepton. If the Higgs boson is heavier than the new particles it can also decay invisibly to \( N \) and \( L \). Note that the presence of new lepton doublets is crucial to our mechanism. One might try to implement our idea replacing the vector-like doublets with SM singlets. This however would imply that the light neutrinos are partially
sterile which in turn would lead to non-universality in weak processes. For instance, the charged-current universality between $\beta$-decay and $\mu$-decay will be modified. As these observables are measured below the 0.1\% level [1], the lower bound on $\overline{M}$ is strengthen, significantly suppressing the BAU. Alternatively, one might study Type-II seesaw models in which Majorana neutrino masses are induced by the VEV of an electroweak triplet scalar boson; but constraints from the precision electroweak data are even more severe.

**Discussion.** In this letter, we showed that the framework of late neutrino masses naturally leads to a viable model of electroweak baryogenesis that can be directly tested in near future experiments.

The additional vector-like leptons with mass close to the EW scale play a crucial role in our scenario. This raises a coincidence problem since a vector-like mass term is unprotected by the symmetries of our model and therefore is unrelated to the EW scale, similar to the $\mu$-problem in the Minimal Supersymmetric SM. There are however many proposed solutions to this problem: vector-like mass may be induced from supersymmetry breaking, additional Higgs fields, or strong dynamics.

The first-order EW phase transition is mandatory. It may be induced, for instance, by higher order terms in the effective potential that arise from integrating out additional heavy states [5].

Our baryogenesis mechanism relies only on physics at the TeV scale, and hence is compatible with any scheme for new physics above the TeV scale. For example there could be flat extra dimensions just above the TeV scale, or a warped extra dimension as in the Randall-Sundrum scheme; in supersymmetric theories our mechanism allows for a low reheating temperature after inflation, solving the coincidence problem since a vector-like mass term is unprotected by the symmetries of our model and therefore is unrelated to the EW scale generically raises many difficulties (Y. Grossman, Nucl. Phys. Proc. Suppl. 105, 315 (2002) [arXiv:hep-ph/0110819]).

We thank K. Agashe, R. Harnik, R. Kitano, Z. Ligeti, S. Oliver, M. Papucci, T. Watari & J. Wells for useful discussions. This work was supported in part by the DOE under contracts DE-FG02-90ER40542 and DE-AC03-76SF00098 and in part by NSF grant PHY-0098840.

---

[1] S. Eidelman et al. [Particle Data Group], Phys. Lett. B 592, 1 (2004).
[2] S. M. Bilenky, Mod. Phys. Lett. A 19, 2451 (2004).
[3] Y. Ashie et al. [Super-Kamiokande Collaboration], Phys. Rev. Lett. 93, 101801 (2004) [arXiv:hep-ex/0404034].
[4] T. Araki et al. [KamLAND Coll.], arXiv:hep-ex/0406035; E. Aiu et al. [K2K Coll.], arXiv:hep-ex/0411038.
[5] P. Minkowski, Phys. Lett. B 67, 421 (1977); T. Yanagida, Proceedings of the Workshop on the Unified Theory and the Baryon Number in the Universe, ed. O. Sawada and A. Sugamoto (Tsukuba 1979); M. Gell-Mann, P. Ramond and R. Slansky, *Supergravity*, ed. P. van Nieuwenhuizen and D. Freedman (North-Holland 1979); R. N. Mohapatra and G. Senjanović, Phys. Rev. Lett. 44, 912 (1980).
[6] C. L. Bennett et al., Astrophys. J. Suppl. 148, 1 (2003) [arXiv:astro-ph/0302207].
[7] M. Fukugita and T. Yanagida, Phys. Lett. B 174, 45 (1986).
[8] See e.g.: W. Buchmüller and M. Pflüger, Int. J. Mod. Phys. A 15, 5047 (2000) [arXiv:hep-ph/0007176]; G. F. Giudice, et al., Nucl. Phys. B 685, 89 (2004) [arXiv:hep-ph/0310123].
[9] Z. Chacko, et al., Phys. Rev. D 70, 085008 (2004) [arXiv:hep-ph/0312267].
[10] N. Arkani-Hamed and Y. Grossman, Phys. Lett. B 459, 179 (1999) [arXiv:hep-ph/9806223].
[11] T. Okui, arXiv:hep-ph/0405083.
[12] H. Davoudiasl et al., arXiv:hep-ph/0502176.
[13] Z. Chacko, et al., arXiv:hep-ph/0405067.
[14] L. J. Hall and S. J. Oliver, Nucl. Phys. Proc. Suppl. 137, 269 (2004) [arXiv:hep-ph/0409276].
[15] H. Goldberg, G. Perez and I. Sarcevic, arXiv:hep-ph/0505221.
[16] There are several interesting low-scale leptogenesis models in the literature (Y. Grossman, et al., Phys. Rev. Lett. 91, 251801 (2003) [arXiv:hep-ph/0307081]; G. D’Ambrosio, G. F. Giudice and M. Raidal, Phys. Lett. B 575, 75 (2003) [arXiv:hep-ph/0308031]; Y. Nagatani and G. Perez, JHEP 0502, 068 (2005) [arXiv:hep-ph/0401070]; A. Abada, H. Aissaoui and M. Losada, arXiv:hep-ph/0409343; A. Pilaftsis, arXiv:hep-ph/0408103; L. Boubekeur, T. Hambye and G. Senjanovic, Phys. Rev. Lett. 93, 111601 (2004) [arXiv:hep-ph/0404038]; A. Pilaftsis, Phys. Rev. D 56, 5431 (1997) [arXiv:hep-ph/9707235]; A. Pilaftsis and T. E. J. Underwood, Nucl. Phys. B 692, 303 (2004) [arXiv:hep-ph/0309342]; T. Hambye, J. March-Russell and S. M. West, JHEP 0407, 070 (2004) [arXiv:hep-ph/0403183]) all of which rely on the late decay mechanism for a departure from thermal equilibrium — they are only indirectly linked with EW symmetry breaking. Furthermore, within the above framework, lowering the leptogenesis scale all the way to the EW scale generically raises many difficulties (T. Hambye, Nucl. Phys. B 633, 171 (2002) [arXiv:hep-ph/0110891]).
[17] L. J. Hall, H. Murayama and N. Weiner, Phys. Rev. Lett. 84, 2572 (2000) [arXiv:hep-ph/9911341].
[18] A. G. Cohen, D. B. Kaplan and A. E. Nelson, Phys. Lett. B 245, 561 (1990); Nucl. Phys. B 349, 727 (1991); P. Hernandez and N. Rius, Nucl. Phys. B 495, 57 (1997) [arXiv:hep-ph/9611227].
[19] M. Berkooz, Y. Nir and T. Volansky, Phys. Rev. Lett. 93, 051301 (2004) [arXiv:hep-ph/0401012].
[20] See e.g.: A. G. Cohen, D. B. Kaplan and A. E. Nelson, Ann. Rev. Nucl. Part. Sci. 43, 27 (1993) [arXiv:hep-ph/9302210]; G. R. Farrar and M. E. Shaposhnikov, Phys. Rev. Lett. 70, 2833 (1993) [arXiv:hep-ph/9305274].
[21] M. B. Gavela, et. al., Mod. Phys. Lett. A 9, 795 (1994) [arXiv:hep-ph/9312215]; P. Huet and E. Sather, Phys. Rev. D 51, 379 (1995) [arXiv:hep-ph/9404302].
[22] A. E. Nelson, D. B. Kaplan and A. G. Cohen, Nucl. Phys. B 373, 453 (1992); Phys. Lett. B 294, 57 (1992) [arXiv:hep-ph/9206214]; S. Y. Khlebnikov, Phys. Lett. B 300, 376 (1993).
[23] E. Braaten and M. H. Thoma, Phys. Rev. D 44, 1298 (1991).
[24] See e.g.: K. Agashe, et al., JHEP 0308, 050 (2003) [arXiv:hep-ph/0308036].
[25] The LEP Collaborations, the LEP Electroweak Working Group, the SLD Electroweak, Heavy Flavor Groups, arXiv:hep-ex/0412015.
[26] See e.g.: M. Raidal and A. Santamaria, Phys. Lett. B 421, 250 (1998) [arXiv:hep-ph/9710389]; Y. Kuno and Y. Okada, Rev. Mod. Phys. 73, 151 (2001) [arXiv:hep-ph/9909265].
[27] F. Vissani, JHEP 9811, 025 (1998) [arXiv:hep-ph/9810435].
[28] See e.g.: C. Grojean, G. Servant and J. D. Wells, arXiv:hep-ph/0407019; D. Bodeker, L. Fromme, S. J. Huber and M. Seni-