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Alloying effects on superionic conductivity in lithium indium halides for all-solid-state batteries

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Alloying of anions is a promising engineering strategy for tuning ionic conductivity in halide-based inorganic solid electrolytes. We explain the alloying effects in Li$_3$InBr$_{6-x}$Cl$_x$, in terms of strain, chemistry, and microstructure, using first-principles molecular dynamics simulations and electronic structure analysis. We find that strain and bond chemistry can be tuned through alloying and affect the activation energy and maximum diffusivity coefficient. The similar conductivities of the $x = 3$ and $x = 6$ compositions can be understood by assuming that the alloy separates into Br-rich and Cl-rich regions. Phase-separation increases diffusivity at the interface and in the expanded Cl-region, suggesting microstructure effects are critical. Similarities with other halide superionic conductors are highlighted. © 2018 Author(s).

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The search for solid-state electrolytes to enable all-solid-state batteries has yielded a number of candidates based on halide anions.1–6 Unfortunately, none of these have been realized commercially, lacking stability to electrodes and voltage or room temperature conductivity matching liquid electrolytes, around $10^{-1}$ S/cm.7 One approach to improving electrolytes is anion alloying. Among superionic conductors, this effect has been demonstrated in the antiperovskites and their analogs,5,6,8 argentides,9 and silver halides,1,10,11 though the effects are often complex or not well described. Indeed, the most conductive alloy composition is difficult to predict since the potential effects of alloying are many. Factors such as strain, local composition gradients, and differences in local Li-anion bond character may be relevant. The role of microstructure must also be considered since phase-separating versus solid solution forming systems can alter materials’ properties in fundamentally different ways.

This letter explores alloying effects on the superionic conductivity of lithium indium halides, Li$_3$InBr$_{6-x}$Cl$_x$, with general implications for other halide alloys. The experimental measurement of conductivities has shown that alloying in Li$_3$InBr$_{6-x}$Cl$_x$ results in a non-monotonic trend, making the material an interesting case study. In particular, the $x = 0$ and $x = 3$ compositions have almost the same conductivity between 300 and 500 K ($10^{-3}$ S cm$^{-1}$ at 360 K), while $x = 2$ has significantly lower conductivity.12

Using first-principles molecular dynamics (MD) simulations, we identify the effect of alloying by simulating four compositions: $x = 0$ (Br$_6$), $x = 2$ (Br$_4$), $x = 3$ (Br$_3$), and $x = 6$ (Cl$_6$), where a shorthand for each composition is given in parenthesis. Among other tools, we leverage our novel bond character analysis, which we recently showed can distinguish between ionic (Coulombic) and polar-covalent character in the Li-halide bond.13 This analysis gives significant additional insight into the chemical effect of alloying. The effect of phase separation is also considered, where strain leads to local concentration gradients that affect ionic conductivity. We find that these chemical, structural, and compositional factors are able to explain the non-monotonic trend in conductivities: Br$_{6-}$$-$Br$_3$$-$Br$_4$$-$Cl$_6$ from highest to lowest.
Superionic diffusivity is due to a small activation energy barrier, $E_a$, and a large maximum diffusion coefficient, $D_0$, through the Arrhenius expression, $D = D_0 e^{\frac{-E_a}{k_B T}}$, where $k_B$ is Boltzmann’s constant and $T$ is the temperature. Our study of Li$_3$InBr$_{6-x}$Cl$_x$ shows that it is necessary to computationally screen for new superionic electrolytes using both $E_a$ and $D_0$. For example, Cl$_6$ has a smaller $E_a$ than Br$_3$, but Br$_3$ has a larger diffusivity at 500 K, due to its larger $D_0$.

Børn–Oppenheimer MD were run on Li$_3$InBr$_{6-x}$Cl$_x$ using the Quantum ESPRESSO plane-wave density functional theory (DFT) code. Using the Nernst–Einstein relationship, the diffusion coefficients, $D$, were calculated. Figure 1 shows example Br$_3$ supercells with the Li-ions removed and an ordered indium (purple) sublattice. A time step of 20 a.u. (0.97 fs) and wave-function and charge density cutoffs of 30 Ry and 300 Ry were used after convergence tests were run. Ultrasoft pseudopotentials for Li, In, Cl, and Br were employed with the Perdew-Burke-Ernzerhof (PBE) exchange-correlation functional. The pseudopotentials are Li.pbe-s-van_ak.UPF, In.pbe-d-rrkjus.UPF, Cl.pbe-n-van.UPF, and Br.pbe-van_mit.UPF.

We independently vary the composition, volume, and microstructure in the MD to isolate the effects of strain and chemistry. The four compositions were simulated as solid solutions with a random placement of Br and Cl in the supercell. For each alloy, the configurational complexity is too great to calculate the full ensemble. Thus, we optimize the geometry of 3–6 reference configurations and simulate the one with the lowest DFT ground state energy. The spread in energies, given in the supplementary material (Table SI.6), is at most 36 meV/atom, within the magnitude of thermal fluctuations at our simulation temperatures. The volumes for Br$_6$ (4389 Å$^3$) and Cl$_6$ (3638 Å$^3$) were optimized, and the Br$_3$ (4112 Å$^3$) and Br$_4$ (4262 Å$^3$) computational volumes were scaled according to the experimental trend in volume versus composition (Fig. 6). The alloyed compositions were simulated at three volumes: 4389, 4262, and 4112 Å$^3$. The computational lattice vectors for each supercell are given in Table SI.1 of the supplementary material. In addition, a nanophase (NP) separated supercell with a Cl-rich side and Br-rich side was simulated for the Br$_3$ composition (right cell in Fig. 1).

All compositions were simulated at multiple temperatures between 500 and 900 K to obtain $E_a$ and $D_0$. MD simulations are equilibrated at temperature and then run for at least 25 ps. Across all compositions and volumes, except Cl$_6$, we see the non-Arrhenius behavior, consistent with our previous study on Li$_3$InBr$_6$. The non-Arrhenius behavior indicates a change in diffusion mechanism and a variable $E_a$. The change in $E_a$ does not occur at the same temperature for all compositions but often occurs between 800 K and 900 K (see Fig. SI.1 of the supplementary material). Thus, we report $E_a$ between 500 and 800 K in Fig. 2.

**Effect of volume and chemistry:** The conventional paradigm of ionic conductivity suggests that diffusivity will increase as volume increases, but for the alloyed systems, the effect is much more profound. Diffusivity in Li$_3$InBr$_{6-x}$Cl$_x$ does not systematically increase with increasing volume because $E_a$ does not systematically decrease. Figure 2(b) shows that Br$_3$ at the central 4262 Å$^3$ volume (yellow) has the highest $E_a$ of that alloy computation, for example. The trend in $D$ can only be understood by also considering the trends in $D_0$. The largest $D_0$ for the Br$_3$ and Br$_4$ alloys occurs at the $\sim$3% expanded volumes [blue for Br$_4$ and yellow for Br$_3$ in Fig. 2(c)]. The far more subtle trend...
FIG. 2. Diffusion coefficients, $D \times 10^6$ cm$^2$/s at 500 K, maximum diffusion coefficients, $D_0 \times 10^3$ cm$^2$/s, and $E_a$ in eV. The white star denotes the computational volume.

in $E_a$, which is a convolution of the size of the octahedral local minima and the tetrahedral transition state, is explored in the supplementary material.

$D_0$ characterizes the shape of the local minimum energy wells (curvature), which we probe by considering the effects of volume and chemistry. We posit that large values of $D_0$ are due to an “ideal” bond length that causes maximum bond frustration, increasing the jump attempt frequency. If Li$^+$ only had purely ionic bonds, it would sit in the center of the halide octahedra and bonds would have no strict angular preferences. In contrast, we previously showed that in Li$_3$InBr$_6$, many Li–Br bonds have polar-covalent character, with a narrower-than expected distribution of angles and shortened bond distances.\textsuperscript{13} Polar-covalent bonds were rigorously defined via distance cutoffs and angle cutoffs based on the centers of Maximally Localized Wannier Functions (MLWF).\textsuperscript{18} In this work, we adopt the same definition and analysis to classify bonds as containing chiefly polar-covalent or chiefly ionic character. Further details on the selection of cutoff criteria can be found in the supplementary material (Figs. SI.1 and SI.2), as well as in Ref. 13.

Bonds in lithium indium halide exhibit frustration in the inability of Li to form simultaneous polar-covalent bonds with all the halides in the octahedral site, which we previously discovered contributes to fast diffusion in Br$_6$.\textsuperscript{13} The octahedral site is too large in Br$_6$, so each Br only has 1–2 simultaneous polar-covalent bonds. Since we no longer consider Li or the halides to be purely ionic, we stop including the charge superscripts.

The ability of Li to form simultaneous polar-covalent bonds depends on the size of the octahedral site, which can be characterized by the distance $r_{X-c}$ from a halide (X) to the centroid (c) in the relaxed supercell (Fig. 3). The distance from Li to the centroid $r_{Li-c}$ depends on the cell volume and the Br/Cl composition; on average, $r_{Li-c}$ is nonzero because of the oscillatory motion and a strong polar-covalent interaction, as described in our previous work.\textsuperscript{13} We compute $r_{Li-c}$ by extracting the Li-halide distance, $r_{Li-X}$, from the Li-X pair correlation function and subtracting $r_{X-c}$. We report $r_{Li-c}/r_{X-c}$ in Fig. 3 and note the increasing trend with volume, contrary to what is expected from purely ionic bonds. At large volumes, Li interacts primarily with one halide, is far from the centroid, and cannot be easily captured in a polar-covalent bond by other halides in the octahedral site, which
The ratio of the Li-centroid distance ($r_{\text{Li-c}}$) to the halide-centroid distance ($r_{\text{X-c}}$) shows that Li stays close to the halide as the volume (in Å$^3$) increases. Purple is for $X = \text{Cl}$, and black is for $X = \text{Br}$. Inset: cartoon of Li close to Br neighbors and the Li-centroid distance indicated with the red line.

affects the jump attempt frequency and thus $D_0$. We point out that similar behavior was observed in AgBr$_x$I$_{1-x}$ alloys, for which silver-halide distances were maintained across large composition regions while distances to the site centroids increased with decreasing $x$.

The Goldilocks effect is observed. If the Li-centroid is too large, Li cannot form simultaneous polar-covalent bonds. If the Li-centroid is too small, Li can form many simultaneous polar-covalent bonds easily. In these extreme simulations, frustration is reduced. The “just right” octahedral size leads to the largest $D_0$ values for each alloy: Br$_4$ with a volume of 4389 Å$^3$ and Br$_3$ with a volume of 4262 Å$^3$ [Fig. 2(c)]. While Br$_3$ with a volume of 4389 Å$^3$ also seems to have an intermediate Li-centroid distance, it is reasonable to expect that the octahedral site is too large using the Br$_6$ volume with a Br$_3$ composition; this $D_0$ has an intermediate value of $6.6 \times 10^4$ cm$^2$/s. The $D_0$ value of the Br$_4$ alloy at the small 4112 Å$^3$ volume could not be easily calculated because the data were severely non-Arrhenius over the range 500-800 K (see the supplementary material), so it is not provided in Fig. 2.

We count the number of polar-covalent bonds that an anion has, on average, for each volume and report the polar-covalent bonds as a percentage of total neighbors in Fig. 4. The general trends in polar-covalent bond character in the alloys are in accord with Fajan’s rules, which state that Br–Li bonds are more polar-covalent than Cl–Li bonds.

We get essential information about the polar-covalent bond strength by examining the effect of the temperature on polar-covalent bonds for Br$_3$. If polar-covalent bonds are competing, simultaneous

![Figure 3](image-url)  
**FIG. 3.** The ratio of the Li-centroid distance ($r_{\text{Li-c}}$) to the halide-centroid distance ($r_{\text{X-c}}$) shows that Li stays close to the halide as the volume (in Å$^3$) increases. Purple is for $X = \text{Cl}$, and black is for $X = \text{Br}$. Inset: cartoon of Li close to Br neighbors and the Li-centroid distance indicated with the red line.

![Figure 4](image-url)  
**FIG. 4.** Percentage of polar-covalent bonds around Br for Br$_3$. The error bars are calculated from the bootstrap sampling method (described in the supplementary material along with a sensitivity analysis).
bonds are tenuous and increasing the temperature can break the bonds. Figure 4 shows a significant change in the number of polar-covalent between 700 and 900 K for the 4262 Å\(^3\) volume, which has the most frustrated Li–Br bonds. Increasing the temperature between 700 and 800 K breaks many of the polar-covalent bonds and helps explain the high \(D_0\). In contrast, the small Br\(_3\) cell has a larger percentage of polar-covalent bonds, which decreases significantly only at 900 K. The large Br\(_3\) cell has a small and constant percentage of polar-covalent bonds. A similar steep trend (not shown) occurs in Br\(_4\) with the 4389 Å\(^3\) volume, which has the highest \(D_0\) for that composition. The trends shown in Fig. 4 are robust with respect to changing the cutoffs defining ionic versus polar-covalent bonds, as described in the supplementary material. Highly frustrated bonds affect \(D_0\) and \(E_a\), contributing to the non-Arrhenius behavior. While frustration in the octahedral site affects \(E_a\), variations in \(E_a\) are more tied directly to the volume of the tetrahedral site, as discussed in the supplementary material.

We find polar-covalent bonds forming at 2.9 Å and 2.65 Å for Li–Br and Li–Cl, respectively, regardless of composition (Figs. SI.1 and SI.2 of the supplementary material). Thus, Li has to be much closer to Cl than Br to form a bond with polar-covalent character. It follows that more Br neighbors lead to increased competition between polar-covalent bonds, which we previously showed to increase the jump rate in Li\(_3\)InBr\(_6\).\(^{13}\)

At the \(x = 3\) composition, most Li ions have 3 Br neighbors. If we define \(\Pi(\text{Br} > 3)\) as the percentage of Li with an excess (>3) of Br neighbors, then the average value of \(\Pi_{\text{ave}}(\text{Br} > 3) = 1.8\%\). However, if we consider only jumping Li, then \(\Pi_{\text{jump}}(\text{Br} > 3) > \Pi_{\text{ave}}(\text{Br} > 3)\) indicates that excess Br neighbors lead to more jumps. This is seen in Fig. 5 which shows \(\Pi_{\text{jump}}(\text{Br} > 3) - \Pi_{\text{ave}}(\text{Br} > 3)\) as a function of temperature and volume. For instance, at 500 K and with a 4112 Å\(^3\) volume, the likelihood for having excess Br neighbors grows for jumping Li by 11.5% in absolute terms. As the temperature or volume increases, the effect of excess Br neighbors decreases because the frustration (competition) between these Li-Br bonds diminishes. Indeed, there is building consensus that frustration, the inability for a system with mobile ions to settle in a significantly deep energy minimum, affects superionic conductivity.\(^9,13,21–23\) Frustrated bonds can set up a chain of correlated diffusion events, further increasing conductivity.

**Effect of phase separation**: Slightly expanded octahedral sites lead to a higher \(D_0\). However, strain can also be induced by a phase separation of Br-rich and Cl-rich regions, either globally or at the nanoscale. We find that the trend in conductivity with alloying\(^12\) is understood by assuming a nanophase (NP) microstructure for the Br\(_3\) composition, which can be directly simulated (Fig. 1).

![FIG. 5.](image) \(\Pi(\text{Br} > 3)\) is the percentage of Li with Br neighbors >3, which leads to more jumps at small volumes and lower temperatures. \(\Pi_{\text{jump}}(\text{Br} > 3) - \Pi_{\text{ave}}(\text{Br} > 3) > 0\) indicates that jumping Li ions are more likely to have excess Br neighbors (Br > 3) than average.
Li$_3$InBr$_{6-x}$Cl$_x$ does not follow Vegard’s Law, which states that the lattice parameter of an alloy is the linear weighted average of the lattice parameters of the parent compounds. Instead there are two trends of volume versus alloying: a Br-rich trend and a Cl-rich trend (Fig. 6). The slope of the Cl-rich region is steep because substituting larger Br anions into the Cl sub-lattice causes the volume to increase significantly. In contrast, substituting a smaller Cl into the Br sub-lattice does not cause as much strain. The abrupt change in slope between the two regimes indicates that the system likely exhibits some phase separating tendency.

The hysteresis in volume upon Cl substitution (red arrows in Fig. 6) after the $x = 3$ composition further suggests the presence of some phase separating tendency. Some of the Cl-rich compositions follow the Br-rich volume-trend, while other samples at the same composition follow the Cl-rich trend. Samples with two different volumes indicate different structures. X-ray diffraction further indicates a phase-separation at the $x = 3$ composition.

Accordingly, we simulated Li diffusion within a NP supercell of Br$_3$ (structure in Fig. 1). Figure 2 shows that at 500 K, the NP at 4262 Å$^3$ has a higher $D$ than the solid solutions of Br$_4$ and Br$_3$ at almost any volume (except for Br$_3$ at 4389 Å$^3$, which is an unphysical ~6% volume expansion). At 500 K, the NP has an order of magnitude higher diffusion than the solid solution and is 3× larger than Li$_3$InBr$_3$Cl$_2$. Thus, Br$_3$ with a nanophase microstructure reproduces the experimental trend in conductivity with alloying: Br$_6$, Br$_3$(NP), Br$_4$, and Cl$_6$ (from largest to smallest). Note that we simulated the NP with a 4112 Å$^3$ volume at 700 K and it has higher diffusivity than the solid solution with the same volume (Table SI.1 of the supplementary material). Thus, we assume that the NP will also have a higher diffusivity than the solid solution with the small volume at 500 K.

We chose to simulate the NP at the medium volume at multiple temperatures because the volume is closer to the relaxed (zero pressure) Br$_3$ volume (see the supplementary material). More importantly, we want to identify the effect of the microstructure on frustration, and the medium volume solid solution Br$_3$ has the highest $D_0$. By calculating the energy of relaxed supercells, we find that the NP has essentially equal energy as the solid solution (Table SI.1 of the supplementary material). Furthermore, the higher diffusivity of the NP microstructure results in a higher cation configurational entropy, which may further stabilize the system. These energy differences support phase separation in the experimental conductivity measurements. As discussed below, the NP material has higher diffusivity at low temperature for two reasons: the expanded volume of the Cl region leads to a higher Li concentration and even higher Li diffusion. Additionally, more Li-ions jump in the interface between the Br and Cl regions.

The expanded NP Cl-region (compared to the Cl$_6$ volume) enriches the Li concentration compared to the Br region. We calculate that the percentage of Li in the Cl-rich side, $\Pi_{\text{Cl-rich}}$, is 8%–9% percentage points larger than the Br-rich side for the simulations at different volumes and temperatures (Table SI.5 of the supplementary material). A similar effect has been discussed in the context of other phase-separating superionic systems, including AgCl/AgI.
FIG. 7. (a) $\Pi_{\text{jump}}(\text{Cl-rich})$ is the percentage of Li in the NP’s Cl-rich region. $\Pi_{\text{jump}}(\text{Cl-rich}) - \Pi_{\text{ave}}(\text{Cl-rich}) > 0$ shows that more jumping Li ions are in the Cl-rich region. (b) $\Pi_{\text{jump}}(\text{interface})$ is the percentage of Li in the interface between the Cl and Br rich regions. Jumping Li ions are more likely to be in the interface than the bulk.

Our analysis at varying temperatures show that the expansion and compression of the Cl and Br regions change $E_a$ and increase or decrease jump events, respectively.

Beyond Li enrichment, Li ions are more likely to jump in the Cl-rich side; $\Pi_{\text{jump}}(\text{Cl-rich})$ is greater than $\Pi_{\text{ave}}(\text{Cl-rich})$. Figure 5(a) shows $\Pi_{\text{jump}}(\text{Cl-rich}) - \Pi_{\text{ave}}(\text{Cl-rich}) > 0$ for all simulations (see also Table SI.5 of the supplementary material). More Li ions jump on the Cl-rich side at small volumes (green > yellow) and lower temperatures. The increase in diffusion in the Br region as the temperature increases supports the hypothesis that $E_a$ is larger in the Br region.

The interface between the Cl-rich and Br-rich regions (the channel in Fig. 1) is also strained. The effects of variations in volume and bond chemistry can lead to frustration of the Li–Br bonds. In the center of the interface, Li has 3 Br and 3 Cl bonds, which is used to distinguish Li in the interface versus the bulk. The percentage of jumping Li in the interface $\Pi_{\text{jump}}(\text{interface})$ is always higher than the average percentage of Li in the interface, $\Pi_{\text{ave}}(\text{interface})$, as shown in Fig. 7(b). $E_a$ in the interface/channel is lower than the bulk, so more jumping occurs at lower temperatures; as temperature increases, the likelihood of jumping in the interface decreases, as expected. Note that the intermediate volume has the largest $\Pi_{\text{jump}}(\text{interface}) - \Pi_{\text{ave}}(\text{interface})$, probably due to the ideal volume for frustrated polar-covalent bonds, similar to the solid solution shown in Fig. 5.

In conclusion, we show how bond frustration and phase separation affect diffusivity in halide alloys. Calculation of $E_a$ and $D_0$ across varying Cl/Br compositions and volumes highlights the importance of a low $E_a$ and a large $D_0$ for superionic conductivity. We find that a large $D_0$ and low $E_a$ can be understood through bond frustration; the effect of strain and chemistry can be controlled through alloying. The “ideal” Li–Br bond length to maximize frustration and thus the jump attempt frequency occurs in Li$_3$InBr$_3$Cl$_3$ at a slightly expanded (3%) volume due to competition between polar-covalent bonds with the Br in the octahedral site. Finally, we show that the experimental trend in the conductivity with alloying can be understood if Li$_3$InBr$_3$Cl$_3$ has a phase-separated microstructure rather than a solid solution. Phase separation has the effect of enriching the Li concentration in the Cl-rich region, creating a space charge layer similar to that proposed for other halide superionic conductors. These insights into halide alloying will provide an important key to finding better and faster solid electrolytes.

See supplementary material for additional information on supercell volumes and energies, diffusion coefficients, octahedral and tetrahedral site sizes, polar-covalent character of bonds, nano-phase Li and jump locations, and geometry optimization.

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