The Relativistic Transactional Interpretation:
Immune to the Maudlin Challenge

June 5, 2018

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Abstract

The Transactional Interpretation has been subject at various times to a challenge based on a type of thought experiment first proposed by Maudlin. It has been argued by several authors that such experiments do not in fact constitute a significant problem for the transactional picture. The purpose of this work is to point out that when the relativistic level of the interpretation is considered, Maudlin-type challenges cannot even be mounted, since the putative ‘slow-moving offer wave,’ taken as subject to contingent confirmation, does not exist. This is a consequence of the Davies relativistic quantum-mechanical version of the direct-action theory together with the asymmetry between fermionic field sources and bosonic fields. The Maudlin challenge therefore evaporates completely when the relativistic level of the theory is taken into account.

1 The Basics: A brief review

The Transactional Interpretation (TI), first proposed by John Cramer [1], is based on the direct-action theory of electromagnetism by Wheeler and Feynman [2]. A relativistic extension of TI has been developed by the present author; that is based on Davies’ direct-action theory of quantum electrodynamics [3]. Due to its possibilist ontology, that model has been termed ‘PTI’ [4], but the important feature is its relativistic nature, which provides further clarification of the conditions for emission and absorption. Therefore, for purposes of this discussion and going forward, I will refer to that model as the Relativistic Transactional Interpretation, RTI.

First, some terminology: in TI and RTI, the usual quantum state |Ψ⟩ is called an ‘offer wave’ (OW), and the advanced response ⟨a| of an absorber A is called a ‘confirmation wave’ (CW). In general, many absorbers A, B, C, ... respond to an OW, where each absorber responds to the component of the OW that reaches it. The OW component reaching an absorber X would be ⟨x|Ψ⟩|x⟩, and it would respond with the adjoint (advanced) form ⟨x|⟨Ψ|x⟩. The product of these two amplitudes corresponds to the final amplitude of the ‘echo’ of the CW from X at the locus
of the emitter (this was shown in \cite{1}) and reflects the Born Rule as a probabilistic weight of the ‘circuit’ from the emitter to absorber and back, the latter being called an incipient transaction. Meanwhile, the sum of the weighted outer products (projection operators) based on all CW responses–each representing an incipient transaction–constitutes the mixed state identified by von Neumann as resulting from the non-unitary process of measurement (cf \cite{4}, Chapter 3). Thus, TI provides a physical explanation for both the Born Rule and the measurement transition from a pure to a mixed state. The additional step from the mixed state to the ‘collapse’ to just one outcome is understood in RTI as an analog of spontaneous symmetry breaking; the ‘winning’ transaction, corresponding to the outcome of the measurement, is termed an actualized transaction. The absorber that actually receives the quantum is called the receiving absorber. This is to emphasize that other absorbers participate in the process but do not end up receiving the actualized quantum.

The other feature of this process, which gives it its possibilist ontology, is that the quantum entities (OW, CW, virtual quanta) are all pre-spacetime objects–Heisenbergian potentiae. Spacetime events only occur as a final result of OW/CW negotiations, resulting in collapse to an actualized transaction. Thus, the collapse is not something that happens within spacetime; rather, collapse is the process of spacetime emergence. Specifically, what emerges as a result of collapse is the emission event, the absorption event, and their connection via the exchanged quantum (see \cite{5}). (This point will be relevant later on.) It is only upon actualization of the transaction that a real quantum is emitted and absorbed at the receiving absorber.\(^1\)

Now let us briefly review the Maudlin thought experiment (\cite{6}, p. 200; see Figure 1). It envisions a ‘slow-moving OW’ (assumed traveling at speed \(v < c\)) emitted at \(t = 0\) in a superposition of rightward and leftward momentum states. On the right at some distance \(d\) is a fixed detector R, and positioned behind R (initially on the right) is a moveable detector L. If, after a suitable time has passed (\(t_1 = \frac{d}{v}\)), there is no detection at R, L is quickly swung around to intercept the OW on the left, where (so the proposal goes) a left-hand CW is generated and the particle must be detected at L with certainty. Thus, this is intended to be a ‘contingent absorber experiment’ (\cite{4}, Chapter 5): it is assumed that the existence of a confirmation from the left-hand side is contingent on the transaction between the source and R failing.

\(^1\)Maudlin is thus quite correct when he says: “It is also notable that in the electromagnetic case the relevant fields are defined on, and propagate over, space-time. The wave-function is defined on configuration space. Cramer does not seem to take account of this, writing always as if his offer and confirmation waves were simply being sent through space. Any theory which seeks to make the wave-function directly a medium of backwards causation ought to take this into account.” \cite{6}, p. 203. This weakness in Cramer’s approach is corrected in RTI.
Maudlin’s intent was to provide a counterexample to the picture provided in [1], in which there are well-defined OW/CW matchups for all possible detection sites. The challenge presented for the original TI was twofold: (i) the probability of 1/2 for the leftward transaction was thought to be inconsistent with the fact that whenever the left-hand CW was present that transaction would always be actualized; and (ii) the situation at $t = 0$ appeared ill-defined, since (if the CW is really contingent as imagined) it is uncertain whether or not the (backward-evolving) CW will be emitted from the left.

Both these concerns have been addressed and resolved elsewhere (cf. [7], [4], Chapter 5). However, these responses assumed that the Maudlin experiment could in-principle be carried out. The purpose of this paper is to observe that in fact this is not the case; no such experiment can actually be done, and therefore the challenge disappears.

2 Applicability of the ‘offer wave’ concept

Since it has been shown that any quantized field theory can be re-expressed as a direct action theory [8], RTI takes all such field excitations as offer waves. That is, any field for which the basic Davies model holds is a component of the transactional model, and transfers of real quanta of those fields can be understood as the result of actualized transactions. However, transactions occur in different ways depending on whether the field is a source of other fields. This issue will be explored in what follows.

In addition, this model has intrinsic restrictions on what sorts of ‘particles’ constitute offer waves. That is, some objects describable as quantum systems, such as atoms, do not constitute offer waves, in that they are not excitations of a specific quantum field–instead, they are bound states [9]. On the other hand, some types of offer waves can participate in actualized transactions indirectly, through confirmations of the products of their interactions, rather than by generating confirmations themselves. This work discusses both these situations, and then applies the findings to the Maudlin challenge to see why it cannot be mounted.
First, as indicated above, the ‘offer wave’ concept refers to the excited states of a quantum field. A specific example would be a one-photon Fock state $|k\rangle$. On the other hand, if the system at hand is not a specific field excitation of this sort, even though it may still be described by an effective quantum state, it is not an offer wave. It therefore does not generate a corresponding confirmation wave. As noted above, an example of such a system would be an atom, which is a bound state of several different quantum fields as opposed to an excitation of a single quantum field.

At this point the relevance for the Maudlin challenge is already evident: the latter proposes a ‘slow-moving quantum’ subject to contingent absorption. The ‘slow-moving quantum’ cannot be anything other than a field excitation for a quantum with nonvanishing mass if it is to constitute an offer wave, so an atom cannot instantiate the experiment. In any case, in the possibilist ontology, OW do not propagate within spacetime at subluminal speeds: they are phase waves, as opposed to group waves. It is only the actualized quantum that propagates at the subluminal group wave velocity—that in itself nullifies the Maudlin challenge. But suppose we overlook that point for now. In order to obtain an offer corresponding to a subluminal quantum, one must use a matter field, such as the Dirac field. The latter will be a source of bosonic fields, which brings us to the second important point: the asymmetry between field sources and their generated fields gives rise to a situation in which a field source participates in transactions only indirectly, by way of its emitted field.

3 Field sources are actualized without matching confirmations

In quantum electrodynamics, the (fermionic) Dirac field is the source of the (bosonic) electromagnetic field, but the following considerations apply to any quantum field and its sources. It is well known that in interactions between fields, the field source has a different physical character from the field of which it is a source. This distinction is reflected in the fact that gauge bosons are the force carriers, as opposed to the fermionic matter fields which are sources of gauge bosons. The asymmetry in question is exhibited for example in the basic QED vertex, which has only one photon line, plus an incoming and outgoing fermion line, due to the nature of the coupling between the Dirac Field and the electromagnetic field, given by $eA_\mu \times \bar{\Psi} \gamma^\mu \Psi$.

![Figure 2: QED Vertex](image-url)
Due to this asymmetry, not all offer waves generate their own confirmations when participating in transactions. Fermionic field sources participate in transactions indirectly, by way of confirmations of the fields of which they are a source. For example (see Figure 2), an electron OW is liberated from a bound state by absorbing an incoming photon from another charged current S, and then emits a photon offer wave, which is confirmed by another charged source field D (typically an electron) in the detector. In the resulting actualized transaction, the associated outgoing electron OW component is actualized as well, even though it was not confirmed by an ‘electron CW’.

The asymmetry between the fermionic field source (the electron E) and its emitted/absorbed fields (the photon lines) is again evident here in that it is an electron propagator that connects to two interaction vertices. This allows the electron E to be indirectly actualized via its interaction with the electromagnetic field. (The doubled photon lines indicate that a CW is generated.) Thus, upon detection of the emitted photon by D, the electron E is actualized without ever having generated its own confirmation.

Even if fermionic quantized fields can be formally recast as direct-action fields, only bosonic fields (subject to a ‘gauge field’ description) engage in transactions by way of their own confirmations. The deep physical meaning behind this is that only the bosonic fields correspond to spacetime symmetries. Thus, when a Dirac field quantum such as an electron is detected, that detection is always indirect, by way of its interaction with the electromagnetic field.

It should be kept in mind that these are all offer wave components, subject to the Born Rule in that they will only be actualized with the corresponding probability. Also, a given process involving particular incoming and outgoing quanta is a superposition of all possible diagrams connecting those incoming and outgoing quanta. Here we consider just the lowest-order diagram for simplicity, but the transaction is a sum of all such diagrams.

The electron propagator is still summed over all possible spacetime locations, as in the usual Feynman diagram calculation. But now we have a reason for the pole in the Feynman electron propagator: it represents the real, as opposed to virtual, electron resulting from an actualized transaction in which real negative charge is transferred from the emitting bound state (cathode) to the receiving bound state (e.g., a conduction band) by way of the actualized incoming and outgoing photons.)
4 OW and CW symmetry

The other new and important feature of the relativistic development of TI (RTI) is that no offer—i.e. quantum state $|\Psi\rangle$—will be emitted in the first place without the basic direct connection (i.e., the time-symmetric field correlation or direct-action propagator) between the potentially emitting system and at least one potentially absorbing system (for details, see [10]). That means that one must have a basic interaction with at least one absorber in order to have an offer at all; such an interaction is a necessary, but not sufficient, condition for an offer to be emitted. The sufficient condition for an offer to be emitted is that a confirmation also exist. Thus, there is no such thing as an isolated OW.

This may seem surprising, but it is because the offer corresponds to a real photon as opposed to a virtual photon (propagator). The only way one can have a real photon in the direct action picture is as a result of absorber response (this is discussed in [10] and implicitly in Davies [3]). The real photon corresponds to the pole in the Feynman propagator, which is only present when there is absorber response (in general, more than one absorber will respond). The pole is what corresponds to a Fock state $|k\rangle$; i.e., an offer wave (or offer wave component). Thus, to get an offer, one always has to have absorber response. This means that the picture of a sequence of stages in which there is first an OW and then one or more CW is not accurate at the fully relativistic level (which is the level at which Nature really operates).

Moreover, since there has been absorber response (usually from many absorbers), technically the correct description of the real photon is the density operator (weighted set of projection operators) corresponding to von Neumann’s ‘Process 1’ (measurement transition). It is only when we consider the emission process by itself, without taking into account that it only occurs because of absorber response, that we label the emission by a ket $|\Psi\rangle$, thinking of it as an independent entity (as in the Maudlin experiment). But it is not. In the direct-action theory, the ket is only a partial description of the process. So it is simply not accurate in the direct-action picture to view an offer as something that is independently emitted; rather, emission is always a two-way process, with the absorber crucially participating in any emission.

5 Why the Maudlin challenge evaporates

Returning now specifically to the Maudlin experiment: in order for the ‘slow-moving quantum’ to be considered an offer, it would have to be a non-composite matter field excitation of some sort, such as an electron state $|\psi\rangle$. The latter is a source of a bosonic field (the electromagnetic field), which is the mediator of electron detection, as described above.\(^5\) Recall that a free electron can neither emit nor absorb a real photon offer wave (due to energy conservation). Thus, an electron subject to detection is always liberated from some bound state (by absorbing electromagnetic energy) and detected via its becoming part of a new bound state (by emitting electromagnetic energy), not through being confirmed by a matching ‘electron confirmation.’ For the latter would mean that it was a free electron.

\(^5\)The weak field is a massive boson, but its range is far too short to be useful for the Maudlin experiment.
To see this, refer again to Figure 2. However, it should be kept in mind that the described processes do not occur in a temporal sequence within spacetime; rather, they occur at the pre-spacetime level, as a negotiation of possibilities. On the incoming side on the left, a photon offer is emitted from another charged current (labelled S) and absorbed by the electron offer E, which is thereby liberated from its initial bound state. Meanwhile, at the outgoing side, E emits another photon offer. The latter is confirmed by a charged current D in the detector, the confirmation propagating back through the electron propagator and actualizing the absorbed photon that liberates E (which is why both photon lines are doubled). The actualization of the emissions and absorptions of both photons actualizes E as an emitter/absorber, since (recall from Section 1) all actualized transactions actualize three things: the emission event, the absorption event, and the transferred quantum. Finally, the outgoing current E becomes incorporated into another bound state (such as a conduction band in a metal) rather than prompting its own confirmation. None of these processes can occur without confirmation of the photon OWs, since (as discussed in the previous section) a necessary condition for a photon OW to exist at all is that a matching CW be generated. A rough analogy is a tug-of-war between two parties: there is no tug-of-war until both parties pick up their respective ends and begin pulling. The ‘possible’ processes described above are just the placing of the rope between them in preparation for the actual game.

So suppose we tried to do the Maudlin experiment with an ‘offer wave’ corresponding to a subluminal electron state. We could arrange for the electron offer to be in a superposition of rightward and leftward directions, but in order to it to be liberated at all, real energy would have to be supplied—i.e., a real photon would have to be absorbed by the bound electron subject to emission. The only way you get a real photon is through absorber response—otherwise you don’t get the pole in the Feynman propagator corresponding to a Fock space state, i.e., the ket that you need for a photon offer wave. And you must have at least two QED interaction vertices for energy conservation. So the entire process presupposes absorber response at the detector end in order for the electron offer ever to be emitted at all. You simply don’t get the electron offer in the first place without the complete photon incipient transaction (i.e., both incoming and outgoing photons must be confirmed). So the situation involving a contingent confirmation never exists; there are always photon confirmations for any offers in play, even if those offers are states of a subluminal fermionic matter field.

6 Conclusion

New developments of the Relativistic Transactional Interpretation (RTI) have been presented which nullify the Maudlin challenge for the Transactional Interpretation (TI). These new development are: (1) offer waves are excitations of quantum fields, so slow-moving composite quantum objects such as atoms are not eligible for the experiment; (2) fermionic matter fields describable as field excitations are not actualized by way of their own matching confirmations, but by confirmations of their emitted/absorbed fields; and (3) a necessary and sufficient condition for the existence of a photon offer wave (OW) is that a confirmation (CW) also be generated. (All these processes involving OW and CW are pre-spacetime processes.) These developments
result in the evaporation of the Maudlin challenge, since there is no ‘slow-moving offer wave’ to begin with, unless it is a non-composite fermion such as an electron. In the latter case, an electron offer is actualized by way of photon OW of which it is a source. And in that process, a condition for a photon OW in the first place is that a photon CW is also generated. Thus, even if we had a slow-moving electron OW, there would always be accompanying photon OW and CW, and there would therefore never be a contingent CW situation—i.e., never a situation in which a CW is only generated based on some prior non-detection. Finally, these observations should not be mistaken as ad hoc maneuvers to evade the Maudlin challenge; rather, they arise directly from the Davies QED absorber theory upon which RTI is based, but had not been previously taken into account.

Acknowledgments. The author is grateful to an anonymous referee for helpful suggestions for improvement of the presentation.

Moreover, according to the possibilist ontology, all OW are phase waves, and they are pre-spacetime objects, so they are not subluminal anyway.
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