Enhanced super-resolution microscopy by extreme value based emitter recovery

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Super-resolution localization microscopy allows visualization of biological structure at nanoscale resolution. However, the presence of heterogeneous background can degrade the nanoscale resolution by tens of nanometers and introduce significant image artifacts. Here we investigate and validate an efficient approach, referred to as extreme value-based emitter recovery (EVER), to accurately recover the distorted fluorescent emitters from heterogeneous background. Through numerical simulation and biological experiments, we validated the accuracy of EVER in improving the fidelity of the reconstructed super-resolution image for a wide variety of imaging characteristics. EVER requires no manual adjustment of parameters and has been implemented as an easy-to-use ImageJ plugin that can immediately enhance the quality of reconstructed super-resolution images. This method is validated as an efficient way for robust nanoscale imaging of samples with heterogeneous background fluorescence, such as thicker tissue and cells.

Significant advance in localization-based super-resolution imaging techniques (also known as STORM, PALM or iPALM)1–4 have revolutionized the field of light microscopy and allows visualization of the previously invisible molecular structures at a resolution of ~20 nm. Their super-resolved imaging capability is achieved by precise localization of individual fluorescent emitters with nanometer accuracy. However, in many biological experiments, the fluorescent emitters can be distorted or obscured by the heterogeneous noisy background, which can introduce inaccuracies up to tens of nanometers. The inaccuracy can significantly compromise the resolution and quality of the reconstructed super-resolution image in forms of image artifact (i.e., misrepresentation of samples’ structure) and localization bias (i.e., shifting the true positions of localized emitters)5–8. Such limitation restricts the application of super-resolution localization microscopy to those thin cells and tissue where the background is relatively uniform. To achieve state-of-the-art super-resolution imaging5,6,8 in a wide variety of biological samples (e.g., thicker tissue and cells), accurate emitter recovery from the heterogeneous background fluorescence is critical.

Earlier attempts to recover fluorescent emitters rely on conventional image processing methods, such as spatial filtering (e.g., rolling ball filter5,9) and temporal filtering (e.g., temporal median filter7,10). These approaches are not based on rigorous estimation models for super-resolution localization microscopy, and all have serious limitations in practice. Spatial filters lack robustness to background structure and emitter size. Temporal median filter suffers from serious over-estimation that can suppress the emitter intensity and size, which can severely reduce the emitter recall rate and affect the localization accuracy, especially in axial dimension7. Recent advances in deep learning is another alternative to estimate the heterogeneous background, however, the overall performance of deep learning based methods highly depends on the training dataset11, and is not trivial for biologists to properly train and optimize all parameters. In our previous work12, we briefly introduced an extreme value based method, EVER, to estimate the heterogeneous background. However, that work only demonstrated EVER’s performance for two-dimensional high-density emitter localization. An extensive assessment on the overall performance of EVER in various scenarios with different imaging characteristics is highly demanded.

Here, we extensively evaluated EVER, an accurate emitter recovery method using an extreme value-based estimation model to correct for heterogeneous background in super-resolution localization microscopy. This method accurately separates the fast-varying emitter signals from the slow varying background signal without restrictions present in conventional methods, and reduce image artifacts and improve the accuracy and fidelity of reconstructed super-resolution images. We demonstrate the superior performance of EVER over conventional methods for a wide range of imaging characteristics using dataset from numerical simulation and biological experiments.
experiments with tissue and cell samples. Moreover, we have implemented EVER as an easy-to-use ImageJ plugin to help the users to immediately improve the performance of their super-resolution localization microscopy.

Results

General description of extreme value based emitter recovery (EVER). The main procedures of EVER can be divided into two steps: (1) segment the raw image stack to a series of image sub-stack along the temporal axis and calculate the pixelwise minimum value for each image sub-stack (Fig. 1a,b); (2) estimate the background from the temporal minima based on their relationship look-up table to recover the emitters (Fig. 1c–e).

The superior performance of EVER can be explained by the extreme value statistics theory. In super-resolution localization microscopy, the acquired composite signal, composed of the fast-changing emitters and the slowly varying background, can be modeled as a Poisson distribution. In an extreme case with ultimate sparse emitter signal, the composite signal is almost the same as the background signal, which can be well estimated by temporal median or mean value and be separated to recover the emitter signal. But in practice, when a much higher emitter density is present in each image frame (e.g. probabilities of emitter signal's occurrence is over 50%), the temporal median or mean value is significantly skewed towards higher fluorescence intensity of the composite signals, indicating its tendency to seriously over-estimate the background. On the other hand, the temporal minimum value is inherently more resistant to varying probabilities of emitter signal's occurrence, suggesting its robustness under different imaging conditions with various emitter densities. However, the temporal minimum value is not equivalent to the actual background signal. A lookup table of their relationship (Fig. 1c) is used to estimate the background signal directly from temporal minimum value and separate emitters from background (Figs. 1d–f).

Validation of EVER against the ground truth of simulated dataset. We first validate the accuracy of EVER against the ground truth using simulated dataset that contains a rather complex imaging characteristics composed of heterogeneous background, various emitter density, size and intensity. The detailed simulation parameters are described in Supplementary Methods. For each simulated dataset, the performance of EVER is benchmarked against the ground truth and two conventional methods—temporal median filter (MED) and spatial rolling ball filter (RB). As shown in Fig. 2, EVER accurately separates emitters from the noisy background, in which the recovered emitters show the best match with the ground-truth image. In comparison, the
recovered emitters by MED exhibit apparent reduction in the intensity and size, due to the over-estimated background; the recovered emitters by the spatial filter of RB exhibit erroneous structures as the artifacts introduced by the heterogeneous background. We further quantify their image similarity of the recovered emitters using EVER, MED and RB, as shown in Fig. 2c. EVER indeed best recovers the emitters with ~98% similarity compared to the ground truth, while other methods only show <60% similarity with the ground truth. The similar performance holds for other imaging scenarios with various background structures, emitter density, emitter size, emitter intensity and emitter shape, as shown in Supplementary Figs. S1–S6.

Performance of EVER on the reconstructed super-resolution image. The accuracy of emitter recovery directly affects the quality of subsequent super-resolution image reconstruction. As shown in Fig. 3, we compared the performance of EVER against the conventional methods of temporal median filtering (MED) and spatial rolling ball filtering (RB) based on the simulated datasets with the known ground truth. Figure 3a shows the simulated single-frame raw image (a1) with three emitters on top of a heterogeneous background, and the recovered emitter images from the ground truth (a2) and using EVER (a3), MED (a4) and RB (a5), respectively. The recovered emitters using EVER (a3) best resemble those from the ground truth (a2). While the emitter images recovered by MED (a4) show much smaller emitter size and lower emitter intensity, and those recovered by RB (a5) show the residual background features. This observation is further confirmed in the corresponding cross-sectional profile shown in Fig. 3c. The red solid line from EVER best tracks the profile from the ground truth (black solid line), but the profile from the MED-recovered image (green) shows the over-estimated background with reduced emitter intensity and size, and the profile from the RB-recovered image (blue) shows the result from the under-estimated background such as the region indicated by the black arrow (Fig. 3c).

Following emitter recovery, we reconstructed the super-resolution images reconstructed by ThunderSTORM, rendered as the 2D image (Figs. 3b,d–e) and the 3D scattered plot of localized emitter positions (Fig. 3d). Without any processing, the heterogeneous background results in many erroneously localized emitters, shown as image artifacts in Figs. 3b1,d1. After EVER, the reconstructed super-resolution image (Fig. 3b3) shows the closest match to the super-resolution image reconstructed from the ground truth (Fig. 3b2). Whereas other methods (MED and RB) suffer from apparent reduction in localization accuracy and image resolution. Table 1 compares the performance of emitter recovery on localization accuracy of the emitter position and size, quantified by localization bias and precision. EVER shows the best localization accuracy, comparable to that from the ground truth.
Experimental results in tissue imaging. To demonstrate the performance of EVER on super-resolution imaging of biological samples, we first used an experimental dataset of imaging heterochromatin from tissue section. Super-resolution imaging of tissue section is especially challenging due to the presence of heterogeneous background.
Experimental results in cell imaging. Although strong heterogeneous background is less common for imaging thin cultured cells, it can be significant in multi-color dSTORM imaging when strong crosstalk (light from one color leaked into another color channel) is present. In our experiment, we labelled the mitochondria with Alexa647 and microtubule with Cy3B and a four-band dichroic mirror and emission filter were used in our microscopy setup (Fig. 5a). Figures 5b1 show strong non-uniform background due to the cross talk from the Cy3B-labeled microtubule when imaging the mitochondria. Figures 5b2–b4 show the recovered emitters by EVER, MED and RB. Similar to our previous findings, the MED-recovered image (Fig. 5b3) shows a significantly smaller number of recalled emitters. Although MED-based recovery eliminates the image artifacts caused by non-uniform background, but sacrifices the emitter intensity, emitter size and recall rate due to the over-estimated background, consistent with our previous simulation and experimental results.

Table 1. Localization bias and precision* of the emitter positions (x-dimension) and size for recovered emitters from the ground truth (TRUE), EVER, MED and RB. The localization bias is defined as the mean value of the localization error, and the localization precision is defined as the standard deviation of the localization error.

| Lateral position | Bias (nm) | Precision (nm) |
|------------------|-----------|----------------|
|                  | Left emitter | Middle emitter | Right emitter |
| TRUE             | 0.4        | 1.5            | 1.9            |
| EVER             | 0.9        | 2.1            | 3.3            |
| MED              | 1.9        | 2.3            | 3.7            |
| RB               | 9.1        | 2.2            | >50            |

| Emitter size | Bias (nm) | Precision (nm) |
|--------------|-----------|----------------|
|              | Left emitter | Middle emitter | Right emitter |
| TRUE         | 0.1        | 0.8            | 3.1            |
| EVER         | 0.1        | 0.9            | 4.9            |
| MED          | 5.0        | 21.3           | 40.6           |
| RB           | 22.9       | 17.6           | >50            |

Computation speed. We also compared the computation speed of different methods using ImageJ (Intel Core i7-4790 @ 3.6 GHz, single thread was used) for our experiment dataset in Fig. 4 (image size: 128X152 pixels, frame number: 20000 frames). Our method (EVER) takes ~ 9 s (~ 2222 fps), RB takes ~ 115 s (~ 173 fps), and MED takes ~ 53 s (~ 377 fps). Therefore, besides the improved robustness and accuracy demonstrated above, EVER is also significantly faster than RB and MED by a factor of 12 and 5, respectively. This speed is sufficient for online analysis for the increasingly large dataset of super-resolution localization microscopy.

Conclusion. In conclusion, we extensively validated an extreme value-based emitter recovery method, EVER, that improves the fidelity and the resolution of super-resolution localization microscopy with a robust performance for a wide range of imaging characteristics. EVER uses a time-domain statistical model that is more suitable than conventional spatial filters to separate the fast-changing emitters from the slowly varying background. It is rather counter-intuitive to use the extreme value for background estimation, as it is traditionally considered to be less accurate compared to temporal median or mean filter in conventional imaging processing. We demonstrate that in super-resolution localization microscopy, the extreme-value-based model exhibits superior robustness.
to separate the fast-varying emitters from the slowly varying background with a simple algebraic relationship to link the temporal minimum value to the actual background signals. We validate the accuracy and robust performance of our method against the ground truth using simulated datasets with a wide range of emitter and background characteristics. We also demonstrate that EVER enables robust and accurate nanoscale imaging in challenging scenarios for super-resolution localization microscopy, such as imaging densely packed structures in tissue slices with heterogeneous bright background and strong color cross-talk, where conventional methods result in image artifacts, compromised image resolution, and reduced emitter recall rate. We implement this method as a super-fast and easy-to-use ImageJ plugin, which can be directly applied to the dataset from sparse, high-density, 3D super-resolution localization microscopy to immediately enhance their image resolution and reduce artifacts without any manual parameter adjustment.

**Methods**

**Theoretical basis and implementation of extreme value-based emitter recovery (EVER).** In modern super-resolution localization microscopy, the most commonly used camera for signal acquisition is sCMOS cameras\cite{16-18}, whose read noise (< 2 electrons), dark noise (generally < 0.1 electrons per frame) and the well-calibrated fixed pattern noise can be neglected. In this situation, the acquired signal can be modeled as Poisson distribution. The recorded composite signal is comprised of the fast-changing emitters and the slowly varying background. In an extreme case with ultra-sparse emitter signal, the recorded signal is predominated by the background signal, the background can be well estimated by using temporal median value\cite{7}. But in the scenario of dense emitters when the probability of emitter occurrence within an imaging sequence is over 50%, the temporal median value is seriously larger than the actual background signal. However, the extreme (minimum) value remains relatively stable regardless of the probability of emitter occurrence, suggesting its inherent robustness. To derive the statistics of temporal minimum, we first consider $N$ random variables to model the photon number $K_1, K_2, ..., K_N$, that is independently and identically Poisson distributed with the probability distribution function (PDF), cumulative distribution function (CDF) given by the following equation:

\[
\text{Figure 4. Performance of our extreme value-based emitter recovery (EVER) for super-resolution localization microscopy. (a1) A single-frame raw image of the heterochromatin (labeled by Alexa 647-conjugated antibody against H3K27me3) from a tissue section in the imaging condition for super-resolution localization microscopy and the recovered emitters and background using EVER (a2), MED (a3), and RB (a4). Scale bar: 4 µm. (b) A wide-field image and the super-resolution image of heterochromatin reconstructed by ThunderSTORM without any additional processing (c1) and with emitter recovery by EVER (c2), MED (c3), and RB (c4). Blue box indicates the image artifact caused by the heterogeneous background. The number of recalled emitters is shown on the upper right corner of each reconstructed image. Scale bar: 2 µm.} \]
where $\lambda$ is the expected average photon number for each pixel. Then we define a new random variable $K_{\min} = \min(K_1, K_2, ..., K_N)$ that takes the minimum value among the N Poisson random variables. The cumulative distribution function of this minimum value is

$$CDF(k, \lambda) = Prob(K \leq k) = e^{-\lambda} \sum_{r=0}^{k} \frac{\lambda^r}{r!}$$

Then the probability mass function (the probability of being the minimum value) is now given by

$$pmf_{\min}(k, \lambda, N) = Prob(K_{\min} = k) = CDF_{\min}(k, \lambda, N) - CDF_{\min}(k-1, \lambda, N)$$

$$= (Prob(K > k - 1))^N - (Prob(K > k))^N = (1 - CDF_{\min}(k - 1, \lambda))^N - (1 - CDF_{\min}(k, \lambda))^N$$

The Eq. (3) assumes uniform background ($\lambda$) over N (frames). However, for many experimental data, the background also undergoes a slow decay during N frames. To account for such variation, we introduce a decay ratio $R$, and Eq. S3 can be modified to Eq. (4)

$$pmf_{\min}(k, \lambda, N, R) = \prod_{n=0}^{N-1} \left( 1 - CDF_{\min} \left( k - 1, \lambda \left( 1 + (R - 1) \frac{n}{N-1} \right) \right) \right)$$

$$- \prod_{n=0}^{N-1} \left( 1 - CDF_{\min} \left( k, \lambda \left( 1 + (R - 1) \frac{n}{N-1} \right) \right) \right)$$

When $R=1$, Eq. (4) is reduced to Eq. (3). The background decay ratio ($R$) is an automatically calculated parameter. In this study, we first separate the background pixels without blinking events by comparing the mean and standard deviation value of the pixel in the temporal dimension of each sub-stack. If the standard deviation value of a specific pixel in the temporal dimension is less than 2 times of the mean value, this pixel is recognized as the background pixel. The decay ratio is then obtained by the following equation:
\[ R = \sum_{f=1}^{N} \frac{I_{bg}(f)}{\min(I_{bg}) \cdot N} \]  

(5)

where \( I_{bg} \) is the average value of the background pixels in each frame of the sub-stack. \( N \) is the frame number of the sub-stack.

An accurate estimate of the minimal value requires that the distribution represented by \( pmf_{\min} \) to have a narrow dispersion around its mean (e.g., with a small standard deviation), which can be achieved by applying a spatial mean filter. The distribution can be described by the following Eq. (6)

\[ pmf_{\min}(k, \lambda, N, R) = pmf_{\min}(k, \lambda, i = 1) \otimes pmf_{\min}(k, \lambda, i = 2) \ldots \otimes pmf_{\min}(k, \lambda, i = m) \]  

(6)

where \( m \) is the number of pixels being averaged. Therefore, Eq. (5) gives the mathematical solution to describe the probability distribution of temporal minima value, given the expected background value. The look-up table to link the background value and the corresponding temporal minimum value is calculated with this equation. Alternative strategies such as using the second minimum value or applying denoising filter (e.g., wavelet filter) to the temporal minimum value map can further improve the precision of EVER.

The ImageJ plugin of EVER can be found on this website: https://github.com/YangLiuLab/EVER-ImageJ-Plugin.

**Numerical simulation.** To mimic a wide range of image characteristics in super-resolution localization microscopy, we simulated a series of image sets composed of spatially non-uniform background and emitters with various emitter density, size and intensity. The image size was set to be 128×128 pixels with a pixel size of 100 nm, and the emitters were randomly distributed in the central 100×100 pixels. For each image frame, the fluorescence signal is modeled as a distribution of emitters convolved with a point spread function and a spatially-varying background:

\[ I(i,j,f) = \text{Poisson} \left[ \sum_{n=1}^{N} (PSF(n) \ast A(x,y,f)) + \text{background}(i,j,f) \right] \]  

(7)

where \( f \) is the frame number, \( (i,j) \) is the coordinate of each pixel on the image, and \( A \) is the intensity of the \( n \)th emitter, \((x, y)\) is the lateral position of the \( n \)th emitter, \( PSF(n) \) is the point spread function of the \( n \)th emitter and \( N \) is the total number of emitters in the image.

**Image reconstruction.** To compare EVER with conventional methods for emitter recovery, the temporal median filter (MED) is implemented following the literature, and rolling ball filter (RB) is implemented by using ImageJ plugin (Process > Subtract background) with a radius of 5 pixels. For super-resolution image reconstruction, ThunderSTORM was used for all the simulation and experiments in this study. Wavelet filter was selected for image denoising and single-molecule least-squares Gaussian function fitting was used for localization. We acknowledge that our method improves the localization accuracy affected by non-uniform background, but it does not improve the localization precision affected by the increased Poisson noise from a high background. Furthermore, as we used least-square Gaussian localization algorithm for our super-resolution image reconstruction, we directly remove the background from our raw image set for the subsequent image reconstruction. However, if maximum likelihood estimator (MLE) is used, the estimated background image is needed for precise calculation.

**Tissue sample preparation.** Immunofluorescence staining of tissue section. A 3 µm-thick tissue section was cut from formalin-fixed, paraffin-embedded (FFPE), de-identified human tissue block of a colon tissue and placed on a No. 1.5 coverslip. The tissue section was first deparaffinized in xylene and rehydrated in ethanol with graded concentration (100%, 95%, 70%, and 50%) and finally in distilled water. Next, heat-induced antigen retrieval was performed in the pre-heated Tris–EDTA buffer solution in microwave oven, then cooled down at room temperature. To block against non-specific binding, the section was incubated with a blocking solution containing 3% BSA and 0.2% Triton X-100 diluted in PBS for 1 h at room temperature. The primary antibody (rabbit polyclonal H3K27me3, Cat. 07–449, Millipore) was diluted to be 1:300 in a solution containing 10 mM glycine, 0.05% Tween 20, 0.1% Triton X-100, 0.1% hydrogen peroxide and 3% BSA in PBS and incubated at 4 °C overnight, followed by Alexa Fluor 647 conjugated goat-anti-rabbit secondary antibody at room temperature for 2 h and then washed with PBS.

**Imaging buffer.** The coverslip that containing the tissue section was glued to a plastic petri dish. The 70% of 2,2-thiodiethanol (TDE, Sigma-Aldrich) in PBS was used to optically clear the tissue section for at least 10 min before imaging. The imaging buffer was prepared fresh by mixing GLOX, 2-mercaptoethanol (βME, Sigma-Aldrich), Cyclooctatetraene (COT, Sigma-Aldrich) and TDE buffer B at a ratio of 1:1:1:98 before imaging. In brief, the GLOX was mixed with 200 µl Buffer A (0.5 mL 1 M Tris (pH 8.0) + 0.146 g NaCl + 50 mL H₂O), 14 mg Glucose Oxidase (Sigma-Aldrich), 50 µl Catalase (17 mg/mL catalase as prepared by dissolving 0.85 mg Catalase in 50 µl Buffer A, Sigma-Aldrich) and TDE Buffer B (2.5 mL 1 M Tris (pH 8.0) + 0.029 g NaCl + 5 g Glucose + 17.5 mL H₂O + 30 mL TDE).

**Cell sample preparation.** MEF cells (ATCC) were maintained in DMEM medium supplemented with 10% FBS. Cells were plated onto a glass-bottom dish (World Precision Instruments, FD3510) at an initial confluency of
50% and cultured overnight to let the cells attach. To perform immunostaining, the cells were first pre-extracted for 30 s in 0.5% Triton X-100 (Triton) in BRB80 (80 mM PIPES, 1 mM MgCl$_2$, 1 mM EGTA, pH = 6.8) supplemented with 4 mM EGTA, washed in PBS, fixed with cold Methanol for 10 min. The cells were then incubated with primary antibodies (rabbit anti-alpha tubulin antibody, abcam 18,251; mouse anti COX IV Mitochondrial antibody, abcam 33,985) at 4 °C overnight. After being washed 3 times with PBS, the cells were incubated with Cy3B-conjugated donkey anti-rabbit secondary antibody and Alexa 647-conjugated donkey anti-mouse secondary antibody for 2 h at room temperature, protected from light. The cells were then washed again 3 times and stored in PBS before imaging. Immediately before imaging, the buffer was switched to the STORM imaging buffer containing 10% w/v glucose (Sigma-Aldrich), 0.56 mg/mL glucose oxidase (Sigma-Aldrich), 0.17 mg/mL catalase (Sigma-Aldrich), 0.14 M β-mercaptoethanol (Sigma-Aldrich).

Super-resolution imaging setup. Our experiments were performed on our home-built super-resolution localization microscopy system. It is built upon an Olympus IX71 inverted microscope equipped with four laser lines including 405 nm (DL405-050, CrystaLaser), 488 nm (DL488-150, CrystaLaser), 560 nm (VFL-P-200–560-OEM1, MPB Communications) and 642 nm (VFL-P-1000–642-OEM3, MPB Communications). Their intensity was controlled by neutral density filters (NDC-50C-4-A, Thorlabs) and high-speed shutters (LS662Z0, Vincent Associates). For super-resolution imaging of tissue section, 642 nm laser with a laser density of 3 kW/cm$^2$ was used for excitation. The four laser beams were expanded by a 10X beam expander (T81-10X, Newport) and combined by the dichroic mirrors and then focused onto the rear pupil of an oil immersion objective (UPLSAPO 100XO, NA = 1.4, Olympus) by an achromatic lens. A highly oblique-angle illumination was used to suppress the background signal. The emitted fluorescence was collected by the objective, passing through the dichroic mirror (ZT488/640rpc-UF1, Chroma) and a band-pass emission filter (ZET488/640 m, Chroma), and then focused by the tube lens and a 0.5X C-mount adapter onto a sCMOS camera (pco.edge 4.2, PCO-Tech), corresponding to a pixel size of 130 nm on the sample plane. A closed-loop piezo nanopositioner (Nano-F100S, Mad City Labs) was used for drift real-time correction tracking the 3D positions of fluorescence nanospheres (f8803, Thermo Fisher Scientific)$^{13}$ Data acquisition, laser intensity control and drift correction were all integrated in our custom-designed software written in LabVIEW (National Instruments) and MATLAB (MathWorks). We acquired 20,000 frames with an exposure time of 20 ms to ensure the collection of sufficient blinking events. For two-color dSTORM imaging of MCF10A cells, the dichroic mirror was replaced by (ZT405/488/561/640rpc, Chroma) and the emission filter is replaced by (ZET405/488/561/640mv2, Chroma). We acquired 10,000 frames with 642 nm laser with a laser density of 3 kW/cm$^2$ at an exposure time of 20 ms to ensure the collection of sufficient blinking events.

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Author contributions
H.M. conceived and developed the EVER method, performed the simulation, data analysis and cell imaging experiment, and wrote the manuscript. W.J. performed the tissue imaging experiment. J.X. prepared the cell sample. Y.L. wrote the manuscript.

Competing interests
The authors declare no competing interests.

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