New Evidence of the Azimuthal Alignment of Quasars Spin Vector in the LQG U1.28, U1.27, U1.11, Cosmologically Explained.

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ABSTRACT

There has been observational evidence about spin axes of quasars in large quasar groups correlated over hundreds of Mpc. This is seen in the radio spectrum as well as in the optical range. There is not yet a satisfactory explanation of this "spooky" alignment. This alignment cannot be explained by mutual interaction at the time that quasars manifest themselves optically. A cosmological explanation could be possible in the formation of superconducting vortices (cosmic strings) in the early universe, just after the symmetry-breaking phase of the universe. We gathered from the NASA/IPAC and SIMBAD extragalactic databases the right ascension, declination, inclination, position angle and eccentricity of the host galaxies of 3 large quasar groups to obtain the azimuthal and polar angle of the spin vectors. The alignment of the azimuthal angle of the spin vectors of quasars in their host galaxy is confirmed in the large quasar group U1.27 and compared with two other groups in the vicinity, i.e., U1.11 and U1.28, investigated by Clowes (2013). It is well possible that the azimuthal angle alignment fits the predicted azimuthal angle dependency in the theoretical model of the formation of general relativistic superconducting vortices, where the initial axially symmetry is broken just after the symmetry breaking of the scalar-gauge field.

Keywords: quasar groups – alignment spin vectors – host galaxy – cosmic strings – scalar-gauge field

1. INTRODUCTION

A large quasar group (LQG) is a cluster of quasars that makes the largest astronomical structures in the current universe. Their sizes can be of the order of hundreds of Mpc. Astronomers believe that a quasar is an active galactic nuclei (AGN) with a vibrant eruption of radiation both optical and in radio range originated by a spinning (Kerr-) black hole, surrounded by an accretion disk. According to Taylor and Jagannathan (Taylor & Jagannathan 2016), a LQG has an internal non-uniform distribution of spin vectors seen in the radio spectrum and the optical spectrum as observed by Hutsemekers et al. (Hutsemekers 2014). This coherence is mysterious and cannot be explained by mutual interaction at the time scale of primordial galaxies formation but rather by use of a more advanced method (Slagter 2018). In a recent study, Slagter (Slagter & Miedema 2021) found that the azimuthal angle of the spin vector of quasars in their host galaxies in six quasar groups, show preferred directions. This is demonstrated through an emergent azimuthal angle dependency of the general relativistic Nielsen-Olesen (NO) vortices at the point after the symmetry breaking at grand unified theory (GUT)-scale. This review focuses on three more other LQG, studied by Clowes (Clowes 2012, 2013).

2. RESULTS
From the NASA/IPAC extragalactic database and SIMBAD we extract for the three LQG U1.11, U1.27 and U.28 the right ascension, declination, inclination, position angle and eccentricity of the host galaxies. The 3-D orientation of the spin vectors can then be calculated (Pajowska 2019). In figure 1 and 2 we plotted the azimuthal angle. Without statistical analysis one can conclude that the preferred orientations are evident. In the case of LQG U1.27 (see table 1 and 2 for the data), we fitted two trigonometric functions on the distribution, which can theoretically be explained (section 3).

\[ V_i = \sum_{n=0}^{\infty} \frac{1}{\omega^n} F_{i}^{(n)}(x, \xi), \]  

where ω represents a dimensionless parameter ("frequency"), which will be large. Further, \( \xi = \omega \Theta(x) \), with Θ a scalar (phase) function on the manifold. The small parameter \( \frac{1}{\omega} \) can also be the ratio of the characteristic wavelength of the perturbation to the characteristic dimension of the background. On warped spacetimes it could also be the ratio of
the extra dimension to the background dimension. In the vacuum case, we expand the metric
\[ g_{\mu\nu} = \bar{g}_{\mu\nu} + \frac{1}{\omega} h_{\mu\nu}(x, \xi) + \frac{1}{\omega^2} k_{\mu\nu}(x, \xi) + \ldots, \]
where we defined
\[ \frac{dg_{\mu\nu}}{dx^\sigma} = g_{\mu\nu,\sigma} + \omega l_\sigma \dot{g}_{\mu\nu}, \quad g_{\mu\nu,\sigma} = \frac{\partial g_{\mu\nu}}{\partial x^\sigma}, \quad \dot{g}_{\mu\nu} = \frac{\partial g_{\mu\nu}}{\partial \xi}, \]
with \( l_\mu = \frac{\Theta}{\omega} \). One then says that
\[ V_i = \sum_{n=m}^{\infty} \frac{1}{\omega^n} F_i^{(n)}(x, \xi) \]
is an approximate wavelike solution of order \( n \) of the field equation, if \( F_i^{(n)} = 0, \forall n \). One can substitute the expansion into the field equations. The Ricci tensor then expands as
\[ R_{\mu\nu} \rightarrow \omega R_{\mu\nu}^{(-1)} + \left( \ddot{R}_{\mu\nu} + R_{\mu\nu}^{(0)} \right) + \frac{1}{\omega} R_{\mu\nu}^{(1)} + \ldots \]
By equating the subsequent orders to zero, we obtain
\[ R_{\mu\nu}^{(-1)} = 0 = \frac{1}{2} g^{\beta\lambda} (l_\lambda l_\mu \ddot{h}_{\beta\nu} + l_\nu l_\beta \ddot{h}_{\mu\lambda} - l_\lambda l_\beta \ddot{h}_{\mu\nu} - l_\nu l_\lambda \ddot{h}_{\beta\mu}), \]
\[ R_{\mu\nu}^{(0)} + \dot{R}_{\mu\nu} = 0, \quad R_{\mu\nu}^{(1)} = 0, \ldots \]
Here we used \( l_\mu l^\mu = 0 \). The rapid variation is observed in the direction of \( l_\mu \). In the radiative outgoing Eddington-Finkelstein coordinates, we have \( x^1 = u = \Theta(x) = t - r \) and \( l_\mu = (1, 0, 0, 0) \), while the bar stands for the background.

3.1. Formation of vortices

In a recent study (Slagter 2016, 2017; Slagter & Miedema 2021) we applied this non-linear approximation scheme on a FLRW spacetime. We considered the matter contribution of a gauged complex scalar (Higgs) field. Physicists
are now convinced that this field plays a fundamental role in the early universe and is responsible for the symmetry breaking in the Standard Model of particle physics. The experimental verification came by the recently observed Higgs particle at CERN. The same field has lived up to its reputation in superconductivity, where the field act as an order parameter to describe the formation of Cooper pairs. The scalar field is combined with a gauge field, parameterized by $A_\mu = \bar{A}_\mu(x) + \frac{1}{\omega} B_\mu(x,\xi) + \frac{1}{\omega^2} C_\mu(x,\xi) + ...$, where we write the subsequent orders of the scalar field as $\bar{\Phi} = \eta \bar{X}(t,r) e^{in_1 \varphi}$, $\Psi = Y(t,r,\xi) e^{in_2 \varphi}$, $\Xi = Z(t,r,\xi) e^{in_3 \varphi}$, with $n_1$, $n_2$, $n_3$ the winding numbers.

### 3.2. The azimuthal angle dependency: breaking the axial symmetry

The azimuthal angle $\varphi$ does not reach the partial differential equations (PDE) in the unperturbed case. By quantum fluctuations, the vortex excite in higher $n$-state and will dissociate into $n$ well separated $n = 1$ vortices, because the energy of the configuration is proportional with $n^2$. The topological characterization is a set of isolated points with winding numbers $n_i$ (the zeros of $\Phi$), with $n = n_1, n_2, ...$. This $n$-vortices solution represents a finite energy configuration. However, an imprint will be left over of the azimuthal dependency of the orientation of the clustering of Abrikosov vortices lattice in the general relativistic situation. So the axial symmetry is dynamically broken. The azimuthal dependency emerge already to first order in the approximation. For example, the energy-momentum tensor $T_{t\varphi} = 0$, while the first order perturbation becomes

$$T_{t\varphi}^{(0)} = \bar{X} \bar{P} \bar{Y} n_1 \sin(n_2 - n_1) \varphi$$

However, in $T_{t\varphi}^{(1)}$ there appears terms like $\cos(n_2 - n_1) \varphi$ and $\sin(n_3 - n_1) \varphi$. The perturbative appearance of a nonzero energy-momentum component $T_{t\varphi}$ can be compared with the phenomenon of bifurcation along the Maclaurin-Jacobi sequence of equilibrium ellipsoids of self-gravitating compact objects, signalling the onset of secular instabilities (Gondek-Rosinska & Gourgoulhon 2002). This shows a similarity with the Goldstone-boson modes of spontaneously broken symmetries of continuous groups. The recovery of the SO(2) symmetry from the equatorial eccentricity takes place at a time comparable to the emission of gravitational waves.

The particular ellipsoid orientation in the frame $(r, \varphi, z)$ expressed as $\varphi_0 \equiv \varphi(t_0)$, is at $t > t_0$ and determined by the transformation $\varphi \rightarrow \varphi_0 - Jt$, where $J$ is the rotation frequency (circulation or "angular momentum") of the coordinate system. The angle $\varphi_0$ is fixed arbitrarily at the onset of symmetry breaking.

1 The stability of the configuration depends on parameter $\lambda$ (Weinberg 2012)
3.3. The pure gravitational radiation case

So far, we found that temporarily off-diagonal terms occurred in the perturbative approach of the Einstein scalar gauge field. What remains unclear is if the breaking of the axially symmetry already appears in the vacuum case like in the vicinity of the black hole spacetime. It is conjectured that the formation of primordial (Kerr-) black holes (and so quasars) happened in the early stages of the evolution of the universe before the stars were formed. Therefore, consider the radiative Vaidya spacetime in Eddington-Finkelstein coordinates

\[ ds^2 = -(1 - 2M(u))/r) du^2 - 2dudr + r^2(d\theta^2 + \sin^2 \theta d\varphi^2), \]

(12)

which is the Schwarzschild black hole spacetime with \( u = t - r - 2M \log(\frac{r}{2M} - 1) \). Here we used \( l_\mu l^\mu = 0 \). In the radiative coordinates, we have \( x^1 = u = \Theta(x) \) and \( l_\mu = (1, 0, 0, 0) \). From Eq.(6) we obtain

\[ h_{rr} = h_{\theta\theta} = 0, \quad h_{r\varphi} = -\sin^2 \theta h_{\theta\theta}. \]

(13)

From the zero-order equations Eq.(7) we obtain

\[ \dot{k}_{rr} = 0, \quad \dot{h}_{\theta\theta} = r\partial_r h_{\theta\theta}, \quad \dot{h}_{\varphi\varphi} = r\partial_r h_{\varphi\varphi}. \]

(14)

So one writes

\[ h_{\theta\theta} = r\alpha(u, \theta, \varphi, \xi), \quad h_{\varphi\varphi} = r\beta(u, \theta, \varphi, \xi), \quad h_{r\varphi} = -r\alpha \sin^2 \theta. \]

(15)

Further, we have

\[ \ddot{k}_{rr} = \frac{1}{r}\left(2\dot{\alpha} \cot \theta + \partial_\theta \dot{\alpha} + \frac{1}{\sin^2 \theta} \partial_\varphi \dot{\beta}\right), \]

\[ \ddot{k}_{r\varphi} = \frac{1}{r}\left(\dot{\beta} \cot \theta - \partial_\varphi \dot{\alpha} + \partial_\theta \dot{\beta}\right), \]

(16)

(17)

\[ \frac{dM}{du} = -\frac{\dot{k}_{\phi\phi} + \sin^2 \theta \partial_{\theta\theta} \dot{k}_{\theta\theta}}{4 \sin^2 \theta} = -\frac{1}{2} \dot{r} h_{uu} - \frac{1}{4} \left(\dot{\alpha}^2 + \frac{\dot{\beta}^2}{\sin^2 \theta}\right) + \frac{1}{4} \left(\ddot{\alpha}^2 + \frac{\ddot{\beta}^2}{\sin^2 \theta}\right). \]

(18)

Not all the components of \( h_{\mu\nu} \) and \( k_{\mu\nu} \) are physical, so one needs some extra gauge conditions. Suitable choice of \( \alpha \) and \( \beta \) (Choquet-Bruhat uses, for example, \( \alpha = 0, \beta = g(u)h(\xi) \sin \theta \)), leads to a solution to second order which is in general not axially symmetric. We can integrate these zero order equations with respect to \( \xi \). One obtains then some conditions on the background fields, because terms like \( \int \dot{\alpha} d\xi \) disappear. From Eq.(18), we obtain

\[ \frac{dM}{du} = -\frac{1}{4\tau} \int_0^\tau \left(\dot{\alpha}^2 + \frac{\dot{\beta}^2}{\sin^2 \theta}\right) d\xi, \]

(19)

which is the back-reaction of the high-frequency disturbances on the mass \( M \). \( \tau \) is the period of \( h_{\mu\nu} \). This expression can be substituted back into Eq.(18). However, in the non-vacuum case, the right-hand side will also contain contributions from the matter fields. In order to obtain propagation equations for \( h_{\mu\nu} \) and \( k_{\mu\nu} \), one proceeds with the next order equation \( R_{\mu\nu}^{(1)} = 0 \). First of all, Eq.(16), (17) are consistent with \( R_{r\varphi}^{(1)} = 0 \) and \( R_{r\theta}^{(1)} = 0 \). Further, one obtains propagation equations for \( \alpha \) and \( \beta \) and for some second order perturbations, such as \( k_{\varphi\varphi} \). Moreover, the \( (\varphi, \theta) \)-dependent part of the PDE’s for \( \alpha \) and \( \beta \) (say \( A(\theta, \varphi), B(\theta, \varphi) \)) can be separated (for the case \( k_{\varphi\varphi} \neq 0 \)):

\[ \partial_\varphi B + 2 \sin \theta \cos \theta A + \sin^2 \theta \partial_\theta A = 0, \]

(20)

\[ \sin^2 \theta \partial_\theta A + 7 \sin \theta \cos \theta \partial_\theta A + 4 \cot \theta \partial_\varphi B + 2(5 \cos^2 \theta - 1) A + 2 \partial_\varphi B = 0. \]

(21)

A non-trivial simple solution is

\[ A = \frac{\cos \theta (\sin \varphi + \cos \varphi)}{\sin^3 \theta}, \quad B = \frac{\sin \varphi - \cos \varphi}{\sin^2 \theta} + G(\theta), \]

(22)

with \( G(\theta) \) arbitrary. So the breaking of the spherically and axially symmetry is evident.

\[ \text{This spacetime is also applied to describe the evaporation of a black hole by hawking radiation in a quantum mechanical way.} \]
4. CONCLUSIONS

There is clear new observational evidence for the azimuthal alignment of the spin vectors of quasars in three new studied LQG. This research presents a new argument about the theoretical explanation of the axial symmetry breaking in a non-linear perturbation scheme considering a vacuum black hole spacetime in radiative coordinates. The recently discovered 13 billion years old quasar P172+18 powered by a supermassive black hole, is all the more reason to believe that the formation of these objects took place in the very early universe.

5. APPENDIX: THE DATA

The data of LQG U1.27 underlying this article are gathered in Table 1 and 2.

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Table 1. Data for the LQG U1.27 (N=71) from NASA/IPAC and SIMBAD. The successive columns represent: right ascension, declination, redshift, inclination, eccentricity, position angle, azimuthal angle and polar angle.

| U1.27 | RA        | Dec        | z     | inc  | ecc  | PA(deg) | ϕ(rad)   | θ(rad)   |
|-------|-----------|------------|-------|------|------|---------|----------|----------|
| 1     | 160.413150| 14.591740  | 1.221 | .830 | .69  | 87      | ± .298   | ± .427   |
| 2     | 160.840103| 14.600057  | 1.271 | .606 | .83  | 113     | ± .371   | ± .427   |
| 3     | 161.128848| 16.045854  | 1.233 | .526 | .87  | 45      | ± .343   | ± .782   |
| 4     | 161.187666| 15.317133  | 1.237 | .741 | .75  | 68      | ± .049   | ± .763   |
| 5     | 161.335962| 14.290068  | 1.270 | .586 | .84  | 63      | ± .063   | ± .678   |
| 6     | 161.516893| 14.044789  | 1.290 | .547 | .86  | 6       | ± .227   | ± .889   |
| 7     | 161.567993| 16.753510  | 1.282 | .772 | .73  | 48      | ± .186   | ± 1.04   |
| 8     | 161.601093| 14.502540  | 1.372 | .660 | .80  | 60      | ± .007   | ± .775   |
| 9     | 162.056815| 14.680304  | 1.290 | .506 | .88  | 170     | ± .82    | ± .215   |
| 10    | 162.248981| 12.889527  | 1.368 | .677 | .79  | 99      | ± .419   | ± .156   |
| 11    | 162.344193| 15.726700  | 1.263 | .772 | .73  | 42      | ± .257   | ± 1.05   |
| 12    | 162.351272| 15.698897  | 1.301 | .435 | .91  | 8       | ± .129   | ± .762   |
| 13    | 162.409269| 21.808144  | 1.235 | .526 | .87  | 33      | ± .127   | ± .849   |
| 14    | 162.423677| 15.306867  | 1.341 | .676 | .79  | 3       | ± .379   | ± 1.00   |
| 15    | 162.449082| 16.371282  | 1.300 | .566 | .85  | 142     | ± .745   | ± .225   |
| 16    | 162.505093| 15.565017  | 1.255 | .357 | .94  | 17      | ± .038   | ± .671   |
| 17    | 162.676146| 16.015594  | 1.269 | .771 | .73  | 125     | ± .744   | ± .340   |
| 18    | 162.767371| 16.316926  | 1.253 | .287 | .96  | 170     | ± .592   | ± .004   |
| 19    | 162.820881| 13.193341  | 1.337 | .483 | .89  | 102     | ± .400   | ± .175   |
| 20    | 162.831696| 14.436524  | 1.315 | .659 | .80  | 54      | ± .084   | ± .812   |
| 21    | 162.845783| 11.981222  | 1.309 | .437 | .91  | 159     | ± .707   | ± .132   |
| 22    | 162.857213| 12.796204  | 1.283 | .641 | .81  | 139     | ± .779   | ± .275   |
| 23    | 162.884258| 14.937553  | 1.367 | .756 | .74  | 94      | ± .354   | ± .211   |
| 24    | 162.918357| 20.655882  | 1.174 | .567 | .85  | 49      | ± .062   | ± .799   |
| 25    | 162.937035| 12.974699  | 1.316 | .461 | .90  | 110     | ± .455   | ± .107   |
| 26    | 163.041780| 16.928818  | 1.339 | .436 | .91  | 59      | ± .077   | ± .576   |
| 27    | 163.092251| 12.515036  | 1.316 | .355 | .94  | 21      | ± .035   | ± .647   |
| 28    | 163.098712| 14.090468  | 1.256 | .622 | .82  | 101     | ± .415   | ± .127   |
| 29    | 163.100377| 20.776172  | 1.203 | .504 | .88  | 25      | ± .160   | ± .827   |
| 30    | 163.190868| 13.682636  | 1.356 | .482 | .89  | 60      | ± .057   | ± .590   |
| 31    | 163.238226| 10.992647  | 1.266 | .483 | .89  | 89      | ± .285   | ± .305   |
| 32    | 163.242363| 20.284854  | 1.253 | .356 | .94  | 41      | ± .026   | ± .611   |
| 33    | 163.552829| 14.959790  | 1.231 | .678 | .79  | 120     | ± .625   | ± .184   |
| 34    | 163.591268| 21.358676  | 1.257 | .606 | .83  | 120     | ± .579   | ± .164   |
| 35    | 163.648532| 10.304548  | 1.260 | .858 | .93  | 16      | ± .084   | ± .671   |
| 36    | 163.677979| 10.722398  | 1.335 | .725 | .76  | 144     | ± .872   | ± .393   |
| 37    | 163.694730| 19.952953  | 1.220 | .566 | .85  | 20      | ± .246   | ± .889   |
| 38    | 163.845984| 13.102997  | 1.358 | .588 | .84  | 11      | ± .295   | ± .889   |
| 39    | 163.854942| 19.298998  | 1.201 | .773 | .73  | 146     | ± .906   | ± .531   |
| 40    | 163.857047| 11.617507  | 1.293 | .527 | .87  | 119     | ± .538   | ± .027   |
| cont. | RA (deg) | Dec (deg) | z | inc | ecc | PA (deg) | $\varphi$ (rad) | $\theta$ (rad) |
|-------|---------|-----------|---|-----|-----|---------|----------------|---------------|
| 41    | 163.924334 | 11.298378 | .845 | .68 | 88  | .249 / .335 | .648 / 1.042 |
| 42    | 163.984288 | 18.788475 | .277 | .355 | .94 | 87      | .262 / .305   | .027 / .683 |
| 43    | 164.046989 | 17.140997 | .344 | .845 | .68 | 72      | .012 / .780   | .505 / 1.066 |
| 44    | 164.091276 | 14.566966 | .243 | .207 | .98 | 129     | .409 / .138   | .412 / -.091 |
| 45    | 164.156218 | 15.013202 | .371 | .787 | .72 | 109     | .541 / .147   | .979 / .483 |
| 46    | 164.158278 | 10.052025 | .273 | .435 | .91 | 128     | .544 / .023   | .507 / .170 |
| 47    | 164.230688 | 14.829509 | .229 | .625 | .82 | 133     | .696 / .257   | .208 / .671 |
| 48    | 164.308435 | 18.798158 | .285 | .382 | .91 | 152     | .614 / .106   | -.133 / .484 |
| 49    | 164.521321 | 20.061417 | .273 | .587 | .94 | 72      | .095 / .549   | .211 / .895 |
| 50    | 164.633936 | 17.082247 | .286 | .462 | .90 | 17      | .175 / .750   | -.139 / .398 |
| 51    | 164.668752 | 17.904320 | .269 | .527 | .87 | 50      | .062 / .700   | .101 / .684 |
| 52    | 164.730550 | 8.230752  | .246 | .677 | .79 | 8       | .401 / .953   | -.025 / .199 |
| 53    | 164.869078 | 16.782794 | .300 | .623 | .82 | 116     | .533 / .122   | .272 / .829 |
| 54    | 165.025092 | 9.444098  | .252 | .567 | .85 | 65      | .019 / .556   | .348 / .666 |
| 55    | 165.070384 | 19.606880 | .240 | .832 | .69 | 114     | .597 / .372   | .423 / 1.040 |
| 56    | 165.166670 | 16.952878 | .300 | .802 | .71 | 127     | .739 / .454   | .354 / .851 |
| 57    | 165.452792 | 8.368669  | 1.196 | .413 | .92 | 9       | .153 / .671   | -.071 / .197 |
| 58    | 165.676552 | 8.655867  | 1.240 | .411 | .92 | 60      | .046 / .481   | .205 / .500 |
| 59    | 166.268588 | 8.759810  | 1.241 | .566 | .85 | 57      | .072 / .606   | .322 / .610 |
| 60    | 166.589189 | 8.868458  | 1.244 | .548 | .86 | 53      | .098 / .618   | .286 / .571 |
| 61    | 166.902560 | 9.020778  | 1.228 | 1.02 | .55 | 87      | .161 / .347   | .860 / 1.175 |
| 62    | 166.935900 | 9.924171  | 1.225 | .383 | .93 | 14      | .143 / .613   | -.071 / .251 |
| 63    | 167.532914 | 10.802888 | 1.211 | .248 | .97 | 129     | .374 / .052   | .006 / .378 |
| 64    | 167.539961 | 7.868564  | 1.208 | .740 | .75 | 10      | .508 / .967   | .015 / .219 |
| 65    | 168.567405 | 10.390996 | 1.210 | .693 | .78 | 151     | .803 / .472   | .168 / .460 |
| 66    | 168.938775 | 8.249943  | 1.194 | .547 | .86 | 106     | .349 / .012   | .381 / .665 |
| 67    | 169.508801 | 10.550690 | 1.215 | .526 | .87 | 134     | .548 / .234   | .196 / .540 |
| 68    | 169.596744 | 9.084715  | 1.197 | .787 | .72 | 98      | .303 / .018   | .620 / .934 |
| 69    | 170.081761 | 8.984773  | 1.229 | .641 | .81 | 56      | .193 / .613   | .373 / .662 |
| 70    | 170.246993 | 10.185907 | 1.208 | .384 | .93 | 77      | .085 / .271   | .196 / .551 |
| 71    | 170.290711 | 7.999635  | 1.141 | .461 | .90 | 93      | .195 / .143   | .320 / .599 |