The Effect of ECAP Processing Conditions on Microstructural Evolution and Mechanical Properties of Pure Magnesium—Experimental, Mathematical Empirical and Response Surface Approach

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Abstract: In this study, a quantitative evaluation approach was used to investigate how certain ECAP processing parameters affect the microstructural evolution, Vicker's microhardness values and tensile properties of pure Mg. The ECAP processing parameters were number of passes, ECAP die channel angle and processing route type. The response surface methodology (RSM) technique was used to design 16 runs of the experiment using Stat-Ease design expert software. Billets of pure Mg were processed up to four passes of routes Bc, A and C at 225 °C. Two ECAP dies were used with internal channel angles of 90° and 120°. Experimental findings were used to establish empirical models to assess the influence of the ECAP processing parameters on grain size and mechanical properties of ECAPed billets. The established relationships were examined and validated for their adequacy and significance using ANOVA as well as several statistical criteria. Response surface plots and contour graphs were established to offer better understanding of the intended relationships. In addition, the optimum processing parameters for grain size, hardness values and tensile properties were defined. Both experimental results and the theoretical model revealed that route Bc is the most effective route in grain refining. The experimental findings showed that four passes of route Bc through the die channel angle 90° revealed a significant reduction in the grain size by 86% compared to the as-annealed counterparts. Similar to the grain size refining, four-passes processing through the ECAP die with an internal channel angle of 90° leads to improved Vicker’s microhardness values. Additionally, four passes of route Bc using the 90° die angle recorded a significant HV increase at the edge and central areas by 112% and 78%, respectively, compared to the as-annealed counterpart. On the other hand, according to the optimization findings, two passes of route Bc resulted in the best ultimate tensile strength for pure Mg, whereas four passes of route Bc revealed the optimum ductility at fracture.

Keywords: severe plastic deformation; equal channel angular pressing; pure magnesium; microstructural evolution; response surface methodology; optimization
1. Introduction

Magnesium (Mg) and its alloys are widely considered ultra-light alloys due to their superior strength to weight ratio. Their densities are two thirds, and one quarter, respectively, of that of aluminum alloys and steel [1–3]. Mg alloys display unique properties, such as high specific stiffness, good recyclability and excellent specific strength, which increase the demand for them in transportation industries [4–9]. Furthermore, the usage of Mg alloys in automotive is an effective means of reducing carbon dioxide emissions and fuel usage. Mg alloys’ high specific strength results in decreased car weights; reducing a car’s weight by 10%, for example, results in saving 5–10% fuel [10]. However, the most significant disadvantage of employing Mg alloys is their low formability. This consequently diminishes their performance in automobile applications.

The available deformation modes of Mg alloys are restricted due to the nature of the Mg crystal’s hexagonal close-packed (HCP) structure [11]. Namely, the significant discrepancy in resolved shear stresses between the slip systems decreases the deformability of Mg alloys [5,12–14]. Therefore, Mg alloys fracture when subjected to traditional deformation methods, such as extrusion and rolling at room temperature [15]. However, Mg alloys’ deformability increases at higher temperatures. The drawback to hot working is that the dynamic recrystallization and recovery processes associated with it mitigate the effects of deformation hardening [16–18]. Several fruitful efforts have been made to develop Mg alloys with useful strength–ductility combinations [19,20] and with better corrosion resistance [20,21]. These attempts to improve Mg alloys’ formability showed that controlling the texture using plastic deformation techniques is a well-suited approach to formability enhancement.

Severe plastic deformation (SPD) techniques have great potential for ambient temperature deformation of Mg alloys [22,23]. SPD includes several techniques applicable to a wide range of materials; one such technique is equal channel angular pressing (ECAP) [24–27]. ECAP possesses several desirable features: its ability to produce ultra-fine-grain (UFG) structures, its capability to fabricate nanostructures efficiently and its applicability to industry [28–31].

Several studies have been investigated to study the ECAP process parameters and their impact on deformation behavior as the mechanical and microstructural characteristics depend on the degree of plastic deformation. The equivalent strain ($\varepsilon_{eq}$) can be theoretically modeled as a function of the die geometry using Equation (1) [31,32]. The strain is affected by the internal channel angle ($\phi$), the outer corner angle ($\Psi$) and number of passes (N).

$$\varepsilon_{eq} = \frac{N}{\sqrt{3}} \left[ 2 \cot \left( \frac{\phi + \Psi}{2} \right) + \Psi \cosec \left( \frac{\phi + \Psi}{2} \right) \right]$$  (1)

Furthermore, the ECAP strain is affected by whether the processed material billets were rotated along its longitudinal axis between passes or not. Different combinations of billet rotations define the ECAP routes. The common ECAP routes are route A, Bc and C. Figure 1 presents the differences among the different ECAP routes. In route A, the rod is not rotated. The rod in route Bc is rotated by 90° between passes. Finally, in route C, the billet is rotated by 180° between subsequent passes [33]. ECAP processing using multiple passes and different routes produces the most grain refinement but also results in significant changes in the shear plane over the entire process [34].
Previous research shows that the compressive mechanical properties of pure Mg deteriorated after the second ECAP pass at room temperature using route Bc and $\phi = 90^\circ$. This reduction is explained by the activation of the non-basal slipping systems, and by the newly formed texture. However, the mechanical properties improved after the fourth pass due to grain refinement [35]. In addition, Venkatachalam et al. [36] applied the ECAP process to the AA2014 aluminum alloy. The mechanical properties were substantially enhanced by processing using route Bc compared to processing via other routes A, C and Ba as the effective strain was homogenized among all the planes. A.I. Alateyah et al. [37] studied the effect of different internal channel angle on the strain homogeneity, microstructural evolution, crystallographic texture and mechanical properties of pure magnesium. The study was conducted experimentally using $\phi = 90^\circ$ and 120° on samples processed for four passes through route Bc at 225°. A numerical finite element analysis approach was conducted using Simufact-forming software. FE simulation showed that the $\phi = 90^\circ$ sample had a more homogenous distribution of stress compared to the 120° one. In addition, investigation of the microstructural evolution and mechanical properties revealed that the $\phi = 90^\circ$ sample showed stronger texture and a higher ultimate strength than the 120° one.

Previous research inquiries optimized ECAP analysis using response surface methodology (RSM). RSM is an empirical set of mathematical and statistical tools that can be used to build, modify and optimize the processes. RSM combines real and modelled responses’ efficiency behavior with a set of effective parameters based on their individual and interactive effects. The RSM is optimized using a genetic algorithm (GA) that avoids localized optimum point uncertainty [38].

Daryadel [39] simulated the ECAP process on the 7075 aluminum alloy with copper casing using the finite element method. RSM was used to design 31 experiments to investigate the effect of four processing (explanatory) parameters on the maximum required force and strain. The simulated results were verified by comparing the experimental and simulation maximum force. On the maximum required force and strain, the effects of four ECAP parameters (channel angle, corner angle, friction coefficient and casing thickness) were investigated. The regression models for computing the maximal forming force and strain are illustrated using analysis of variance (ANOVA).
concluded that channel angle affects resultant force the most. Similarly, the strain was affected by channel and corner angle, and the friction coefficient and the thickness of copper on strain had no significant effect. Finally, the predicted optimal ECAP conditions for reducing the maximum forming force and increasing the strain were 93.64°, 0°, 0.001 and 1.62 mm for channel angle, corner angle, friction coefficient and casing thickness, respectively. Abbas et al. [40] investigated the machining processes of recycled billets Al6061 chip. The billets underwent a three-step process: cold compact, hot extrusion and, finally, ECAP to improve the mechanical properties. Surface roughness and metal removal rate were measured as performance characteristics against various cutting parameters and the number of ECAP passes. The authors concluded that feed was the most influential parameter on the generated surface. Optimum values of MRR and generated surface roughness were obtained using a desirability function approach. The minimum values of surface roughness and maximum MRR were obtained at a cutting velocity of 195 m/min, a feed of 0.073 mm/rev, a depth of cut of 0.4 mm and three passes of ECAP process.

Under RSM, central composite design (CCD) is used for modelling and optimization. To optimize the response performance of any process without localized uncertain optimum point confusion, CCD, desirability function (DF) and GA can be used [38]. Many studies have used GA and hybrid RSM-GA to optimize the process condition. Deshwal et al. [41] investigated the tensile strength of a PLA-fabricated part produced by fused deposition modeling (FDM)—a powerful 3D printing technique—using a statistical technique equipped with numerous hybrid static tools. The contribution of each of the FDM parameters (infill density, temperature and speed) on the maximum performance tensile strength was investigated. To optimize FDM process parameters, hybrid optimization approaches, such as genetic algorithm-artificial neural network (GA-ANN), genetic algorithm-response surface methodology (GA-RSM) and genetic algorithm-adaptive neuro fuzzy interface system (GA-ANFIS), are used. The author concluded that the percentage accuracies of GA-ANN, GA-RSM and GA-ANFIS are 99.89%, 99.3% and 99.55%, respectively. Moreover, the maximum tensile strength of PLA obtained by GA-ANN was 47.0212 MPa, and the optimal conditions were infill density 100 %, temperature 210°C and speed 124.778 mm/s.

A limited number of studies examining ECAP performance numerically were found. However, the experimental studies investigating the effect of ECAP process on pure Mg are limited due to its poor deformability, and mostly focus on ECAP of Mg alloys at $\phi \leq 90^\circ$. Therefore, the present study investigates the ECAP conditions necessary for optimum performance characteristics. These characteristics are grain size ($G_R$), hardness measurement at two positions of specimen: center ($H_C$) and edge ($H_E$), and tensile characteristics, namely ultimate tensile strength ($\sigma_u$) and ductility (D). In addition, an experimental investigation is conducted on pure Mg under various ECAP conditions, such as number of passes (N), ECAP die angle ($\phi$) and the type of processing route. A complete analysis of ECAP’s effect on microstructural evolution and mechanical properties was considered. The research’s design is based on RSM, which is used to identify the optimum ECAP parameter levels by analyzing the impact of ECAP conditions on responses. A second-order regression model and analysis of variance (ANOVA) were created to analyze the ECAP condition of optimum responses. GA was applied to optimize the ECAP condition. Finally, hybrid RSM-GA was created to improve the optimization of ECAP responses, and corresponding conditions were evaluated using GA.

2. Materials and Methods

2.1. Experimental Design

In this study, the effect of 3 ECAP parameters on pure Mg’s microstructure and mechanical properties are investigated. The 3 parameters are: number of passes (N), ECAP die angle ($\phi$) and the type of processing route, as shown in Table 1. In this investigation, the combinations of ECAP parameter values used were designed using response surface methodology (RSM). A total of 16 runs were carried out to investigate various ECAP
responses. The explanatory variables are grain size (GR), hardness measurements at the center (HC) and edge (HE) of the specimen and tensile characteristics—namely ultimate tensile strength (σu) and ductility (D). Experimental data obtained from the microstructural evolution, Vicker’s hardness and tensile tests are shown in Table A1 in Appendix A. The RSM technique was used to analyze three factors with a small number of tests in order to model a second-order response surface. After that, the genetic algorithm is employed to figure out which fitness value is the best.

Table 1. ECAP parameters levels.

| ECAP Parameters          | Parameters Levels |
|--------------------------|-------------------|
| Number of passes (N)     | L1  | L2  | L3  |
| ECAP die angle (φ)       | 90  | 120 |     |
| Processing route type    | A   | Bc  | C   |

2.2. Material and Methodology

In the present study, rolled billets of pure Mg 20 mm in diameter and 60 mm in length were used. Before ECAP processing, the billets were annealed at 250 °C for 1 h, followed by furnace cooling. The pure Mg billets were deformed by ECAP at 225 °C with different numbers of passes (1, 2 and 4 passes) through different routes (A, Bc and C), with 0.05 mm/s ram speed. The ECAP die consists of two channels intersecting with an outer die angle (ψ) of 20° and with different inner angles ϕ (90° and 120°). A graphite-based lubricant was used to reduce friction between the billets and die walls. The samples after ECAP processing were centrically cut along their LS along the plane perpendicular to the die entry channel and parallel to the flow plane (pressing direction). The reference axes were labeled according to the ECAP direction: the transversal direction “X” (TD), the normal direction “Z” (ND) and “Y” (ED).

Microstructural and crystallographic texture of Mg billets after ECAP were studied using a field emission scanning electron microscope (FESEM, Hitachi, Ltd., Tokyo, Japan) that is equipped with a NordlysMax2 electron back-scatter diffraction (EBSD) detector. EBSD was performed on the top surface, the TD-ED plane, using a SU-70 SEM (Hitachi, Ltd., Tokyo, Japan) operating at 15 kV and with a typical current of 1.5 nA. The samples’ surfaces were prepared before the EBSD by grinding and mechanically polishing down to 1 µm using a tripod polisher, then polished chemically with colloidal silica (0.05 µm) for 24 h. by a BUEHLER Vibrometer (Buehler, Tucson, AZ, USA).

Mechanical characterization of the ECAPed samples was measured using the Vickers micro-hardness tester (Shimadzu HMV-FA) under a load of 1 kg for a loading time of 15 s. Additionally, tensile properties at room temperature were measured using uniaxial tensile tests conducted by a universal testing machine (Instron 4210, Norwood, MA, USA) at a strain rate of 10⁻³ s⁻¹. Dimensions of tensile samples were set based on the E8M/ASTM standard. Three specimens per ECAP processing condition were tested to confirm the accuracy of the results. Tensile specimens were sectioned from the center of the ECAPed rods.

2.3. Regression Model

Response surface methodology (RSM) is a powerful tool used to formulate, model, analyze, design and improve optimization processes by a set of statistical and mathematical tools. RSM consists of three main steps. First, conducting multiple runs of the experiment technique with different ECAP process parameters values. Second, developing an appropriate interaction between ECAP response and input factors by regression modelling. Finally, optimizing to identify the contribution of each ECAP process parameter on the appropriate output ECAP response [42,43]. The regression model provides the interaction between the
process response and explanatory variables by fitting them into a second-order polynomial equation [44].

Stat-Ease Design Expert software (version 13.0.5, Stat-Ease, Inc., Minneapolis, MN, USA) is a useful tool for optimizing complicated systems for scientific and industrial applications and was, therefore, used to analyze the experimental data [45,46]. The regression transformations available from Design Expert include linear, square root, natural logarithm, logarithmic with base 10, inverse square root, inverse, power, logit and arcsine square root.

In this study, ECAP parameters were classified into numeric parameters, such as N and ϕ, and categorical parameters, such as processing route. To transform the categorical parameters to numerical ones, dummy coding and binary coding were utilized. In many forms of estimating models, such as linear regression, dummy coding is one approach of using categorical predictor variables. It also uses only ones and zeros to transmit all of the necessary information regarding group membership. Dummy variables are the coded categories that are generated for a category variable. A combination of K-1 dummy variables is required to develop mutually exclusive and comprehensive dummy variables that represent a certain categorical variable with K groupings [47]. For categorical variables route A, route Bc and route C, the dummy variables were coded by X₁ and X₂, as shown by matrix in Equation (2). If X₁ = 1 and X₂ = 0, then the route type is A; if X₁ = 0 and X₂ = 1, then the route type is Bc and if X₁ = 0 and X₂ = 1, then the route type is C.

\[
\begin{bmatrix}
A \\
Bc \\
C
\end{bmatrix} = \begin{bmatrix}
1 & 0 \\
0 & 1 \\
0 & 0
\end{bmatrix}
\] (2)

Many trails of regression transformation from and interaction between independent variables were examined in order to model the output responses of ECAP. The best regression coefficient (R²) indicates that the models generated in the experimental research are statistically significant.

2.4. Genetic Algorithm (GA)

Genetic algorithms (GA) have been used in science and engineering as an intelligent and efficient method for addressing real-world optimization problems in a cost-effective approach. In each individual, the genetic algorithm generates an optimization algorithm and a random number of generations, whereas conventional algorithms generate only a single point and use a deterministic rule to determine the next generation. Every individual’s fitness function is assessed in each generation. The GA uses criteria to determine a global minimum value for a fitness function and ensures that the result converges [43,48].

3. Results and Discussion

3.1. Microstructural Evolution

In the current study, EBSD was used to characterize the microstructural evolution of as-annealed Mg (AA-Mg) after ECAP processing to study how it was affected by the different processing parameters. Figure 2 illustrates the inverse pole figure (IPF) maps of the AA-Mg and the ECAPed samples using route Bc for one pass (1P) and four passes (4P), with different die angles, ϕ = 90° and 120°.

The IPF map of AA-Mg clearly shows that it has inhomogeneous coarse grains, as presented in Figure 2a, after the first ECAP pass grain refinement was observed, regardless of die angle. However, using die angle 90° led to higher refinement, as shown in Figure 2b. This can be argued to relate to the higher strain experienced using the 90° die angle relative to that experienced using the 120° die angle [37]. Table 2 illustrates the grain sizes corresponding to each number of passes and to each die angle through route Bc. Increasing the number of passes up to 4P resulted in even further refinement as the grain size reduced from 1.492 to 0.88 μm using ϕ = 90° and from 2.62 to 1.896 μm using ϕ = 120°.
corresponding to each number of passes and to each die angle through route Bc. Increasing the number of passes up to 4P resulted in even further refinement as the grain size reduced from 1.492 to 0.88 µm using \( \phi = 90^\circ \) and from 2.62 to 1.896 µm using \( \phi = 120^\circ \).

**Figure 2.** EBSD inverse pole figure (IPF) maps for the AA-Mg (a), and after the ECAP processed using route Bc for different passes, (b,c) 1P, (d,e) 4P, with different die angle, \( \phi = 90^\circ \) (b,d) and \( \phi = 120^\circ \) (c,e).
Table 2. Grain size (GR) of AA-Mg and after ECAP process through route Bc using two different die angles (ϕ).

| Data, µm            | AA-Mg | Route Bc                                                                 |
|---------------------|-------|--------------------------------------------------------------------------|
|                     |       | 1P   | 4P   | 1P   | 4P   |
| Min. grain size     | 1.106 | 0.507 | 0.505 | 0.21 | 0.81 |
| Max. grain size     | 34.02 | 9.291 | 22.727| 7.14 | 20.15|
| Average grain size  | 6.338 | 1.492 | 2.62  | 0.88 | 1.89 |
| Standard deviation  | 5.815 | 0.945 | 1.433 | 0.73 | 1.11 |

Figure 3 presents the IPF maps of the 2P ECAPed samples using routes A and C. It is shown that the route A sample contains coarser grains than route C as the maximum grain sizes were 22.62 µm and 11.052 µm, respectively. However, the average grain size was approximately the same, 1.492 µm and 1.374 µm, in route A and C, respectively.

Equation (3) represents the predicted linear model of Mg’s GR based on data from the experiments. The regression coefficient of grain size is \( R^2 > 0.9934 \), and the adjusted value of \( R^2 \) is 0.9889. Figure 4 presents a comparison between predicted and actual GR.

\[
GR = 0.570139 - 0.649646 \times N + 0.0204069 \times \varphi - 0.12025 \times X_1 - 0.261167 \times X_2 + 0.00261528 \times N \times \varphi + 0.0249236 N^2
\] (3)

In addition, the three-dimensional plot, Figure 5, illustrates \( GR \) as a function of \( N \) and \( \varphi \) through the different studied routes. For routes A, Bc and C, the increase in ECAP die angle results in an increase in \( GR \), which lies in good agreement with the experimental results. On the contrary, there is an inverse relationship between the number of passes and \( GR \). The minimum optimum \( GR \) was obtained at four passes and 90° ECAP die angle. The values of \( GR \) are 0.98 µm, 0.88 µm and 1.22 µm for route A, Bc and C, respectively, as shown in Figure 5.
3.2. Mechanical Properties

Vicker’s microhardness tests across the central and edge regions of the ECAPed billets were used to evaluate the homogeneity of hardness. The hardness values of the ECAPed Mg billets processed via route Bc are plotted in Figure 6a as a function of the number of passes, with the different internal die angles taken into account. Figure 6a shows that the AA-Mg hardness significantly increased with increasing the number of passes in both the central and edge areas. The 90° die recorded higher HV-values in the central and edge areas. The 90° die revealed an increase in the HV by 84% at the edge and 50% at the central regions, respectively, compared to the 120° die angle. 90° die angle showed an increase in the HV by 15% and 8% at the edge and central regions, respectively, compared to the 120° die angle recorded a significant HV increase at the edge and central areas by 112% and 78%, respectively, compared to the AA-Mg counterpart. Comparatively, the 4Bc condition of the 90° die displayed 8% and 9% increase in the HV-values at the edge and central regions, respectively, compared to the 120° die counterparts. This discrepancy can be argued to relate to the grain refinement mentioned above. Finally, a conclusion can be drawn that the increasing plastic strain up to 4Bc using the 90° die angle recorded a significant HV increase at the edge and central areas by 112% and 78%, respectively, compared to the AA-Mg counterpart. Comparatively, the 4Bc condition of the 90° die displayed 8% and 9% increase in the HV-values at the edge and central regions, respectively, compared to the 120° die counterparts. This discrepancy can be argued to relate...
to the grain refinement mentioned above. Finally, a conclusion can be reached that strain hardening assisted in enhancing the HV-values with increasing the passes number.

Figure 6. Mechanical properties of the AA-Mg after ECAP process at the different conditions; effect of number of passes and die angle using route Bc (a,b), and effect different routes, A, C and Bc using ϕ = 90° for two passes (c).

Equations (4) and (5) show the predicted modeling of the inverse of \( H_C \) and \( H_E \). The regression coefficients of \( H_C \) and \( H_E \) are 0.9657 and 0.9741, respectively.

\[
\frac{1}{H_C} = 0.0171726 - 0.000110407 \times N + 0.000107254 \times \varphi - 0.000901199 \times X_1 - 0.00320891 \times X_2 - 0.00000961846 \times N \times \varphi + 0.000507579 \times N \times X_2
\]

\[
\frac{1}{H_E} = 0.0159481 - 0.000941798 \times N + 0.0000850833 \times \varphi - 0.00033721 \times X_1 - 0.000736064 \times X_2 - 0.000014373 \times N \times \varphi + 0.000288905 \times N^2
\]

Figure 7 compares actual and predicted hardness values at central and edge areas. Moreover, Figure 8 shows a three-dimensional response surface plot of \( H_C \) and \( H_E \) responses against \( N \) and \( \varphi \) at a constant processing route. For routes A, Bc and C, the increase in ECAP die angle resulted in a decrease in both \( H_C \) and \( H_E \). On the contrary, there is a proportional relationship between the number of passes and both \( H_C \) and \( H_E \). The maximum optimum \( H_C \) and \( H_E \) were obtained at four passes and 90° ECAP die angle. The optimum \( H_C \) values are 52.8 HV, 46 HV and 43 HV for route A, Bc and C, respectively, while the maximum values of \( H_E \) are 46.5 HV, 55 HV and 51.2 HV for route A, Bc and C, respectively.
Tensile tests were conducted for AA-Mg before and after ECAP processing with the different studied conditions. The ultimate tensile stress ($\sigma_u$) and ductility (D) of the ECAPed samples are plotted in Figure 6b,c. As seen in Figure 2, increasing the ECAP passes results in a significant reduction in grain size, which consequently increases the ultimate strength. Figure 6b shows that, using $\phi=90^\circ$, the 1P sample showed an enhancement in $\sigma_u$ by 58%; however, ductility was decreased by ~35% compared to the AA-Mg counterpart. On the other hand, 1P at $\phi=120^\circ$ resulted in a rise in $\sigma_u$ by 44%. Increasing the number of ECAP passes up to 4P showed additional enhancement in the
\( \sigma_u \) by 15\% compared to 1P counterpart. The 4Bc condition yielded further improvement in \( \sigma_u \) by 16\% and a decline in ductility by 10\%. Finally, using routes A, C and Bc resulted in increase in \( \sigma_u \) by 64\%, 71\% and 79\%, respectively, compared to AA-Mg.

The increase in \( \sigma_u \) is a direct consequence of the ultra-fine grains, which can be described using Hughes’ theoretical model [49]. The imposed strain from ECAP processing leads to dislocation motion. As the strain increases, more and more dislocations are absorbed by the low-angle grain boundaries, gradually transforming the low-angle grain boundaries into stable high-angle grain boundaries. Therefore, the grains are refined because of the high-angle grain boundaries formation. However, severe plastic deformation techniques, such as ECAP processing, led to high dislocation density, which delayed the dislocation mobility [50–57], consequently improving the hardness and tensile strength of the ECAPed AA-Mg billets.

Moreover, the significant grain refinement provides the grain boundary strengthening mechanism, thus enhancing the mechanical properties in good agreement with Ref. [58]. As mentioned above, using \( \phi = 90^\circ \) led to finer grain size compared to \( 120^\circ \), which resulted in higher ultimate strength. However, the ductility reduction obtained in \( \phi = 90^\circ \) and \( 120^\circ \) with increasing the number of passes was attributed to smaller grains size, which led to increasing the grain boundary area per unit volume. Consequently, increasing the strengthening results in ductility drop, and similar findings were mentioned in previous work [59]. However, \( 120^\circ \phi \) showed higher ductility compared to \( 90^\circ \) die, as presented in Figure 6b, which could be argued that the lower strain occurred when using the \( 120^\circ \) die angle compared to \( \phi = 90^\circ \).

In addition, the tensile responses of Mg specimen are \( \sigma_u \) and D\%. Equations (6) and (7) represent the linear modelling of tensile response. The regression coefficients of \( \sigma_u \) and D\% are 0.9948 and 0.9752, respectively.

\[
\sigma_u = -553.75000 + 324.62500 \times N + 5.15000 \times \phi + 736.00000 \times X_1 + 207.50000 \times X_2 - 1.42500 \times N \times \phi - 75.50000 \times N \times X_1 - 49.75000 \times N \times X_2 - 4.82500 \times \phi \times X_1 - 22.87500 \times N^2
\]

\[
D = 68.26667 - 8.10000 \times N - 0.353333 \times \phi - 6.90000 \times X_1 - 13.40000 \times X_2 - 0.143333 \times N \times \phi + 0.056667 \times \phi \times X_1 + 0.103333 \times \phi \times X_2 - 1.41667 \times N^2
\]

The relationships between the actual and predicted responses \( \sigma_u \) and D are shown in Figure 9. In addition, Figure 10 shows the three-dimensional interaction effect of ECAP parameters on \( \sigma_u \) and D while generating interaction graphs and response surface plots between two variables at constant processing route. For route A, Bc and C, there are slight effects of ECAP die angle on \( \sigma_u \) of specimen. However, there are different relations between the number of ECAP passes and \( \sigma_u \) in each route. For route A, increasing ECAP number of passes will decrease the \( \sigma_u \). The maximum \( \sigma_u \) at route A (330 MPa) was obtained at four passes and \( 90^\circ \) die angle.

![Predicted vs. Actual](image1)

![Predicted vs. Actual](image2)

**Figure 9.** Predicted and actual value of ECAP responses \( \sigma_u \) (a) and D (b).
Moreover, analysis of variance (ANOVA) is used to examine independent parameters, N, \( \phi \), \( X_1 \) and \( X_2 \), in order to determine which ones have a significant impact on performance parameters, \( G_R \), \( H_C \), \( H_E \), \( \sigma_u \), and D [60]. The significant effects with \( p \)-values less than 0.05 indicate that the independent parameters, as well as the individual model coefficients and interaction terms, are statistically different from zero at the 95% confidence level [61]. Table 3 presents the significant parameters of the five responses after eliminating the insignificant effects using multiple regression analysis on experimental data.

Table 3. Significant independent parameters for each ECAP response.

| Response | Significant Effect |
|----------|-------------------|
| \( G_R \) | N, \( \phi \), \( X_1 \), \( X_2 \), N \( \phi \) |
| \( H_C \) | N, \( \phi \), \( X_2 \) |
| \( H_E \) | N, \( \phi \), \( X_3 \), N \( \phi \), N\(^2\) |
| \( \sigma_u \) | \( \phi \), \( X_1 \), \( X_2 \), N \( \phi \), N \( X_1 \), N \( X_2 \), \( \phi \) \( X_1 \), N\(^2\) |
| D | \( \phi \), \( X_2 \), N \( \phi \), \( \phi \) \( X_2 \), N\(^2\) |

Table 4 presents the statistical tests, namely F-value, \( p \)-value, lack of fit, adequate precision, regression coefficient (\( R^2 \)), adjusted \( R^2 \) and predicted \( R^2 \) of the five models. The F-value is the difference between the variation attributed to individual factors and the variance due to the error...
term. F-values of ECAP responses greater than 4 indicate that changing an input ECAP parameter has a significant impact on the response quality criterion [62]. Die angle has the greatest impact on $G_R$, $H_C$ and $D$. Otherwise, number of passes and route type have a significant effect on $H_E$ and $\sigma_u$, respectively.

Table 4. Statistical tests of ECAP responses.

| Response | F-Value ($F > 4$) | Model Significant ($p < 0.05$) | Lack of Fit ($p > 0.05$) | Adeq Precision (Ratio $> 4$) | $R^2$ | Adjusted $R^2$ | Predicted $R^2$ |
|----------|------------------|--------------------------------|--------------------------|---------------------------|------|---------------|----------------|
| $G_R$    | 224.52           | 0.0001                         | 0.1395                   | 41.3955                   | 0.9934 | 0.9989        | 0.968          |
| $H_C$    | 42.22            | 0.0001                         | 0.4739                   | 17.4906                   | 0.9657 | 0.9428        | 0.895          |
| $H_E$    | 56.44            | 0.0001                         | 0.0659                   | 22.39                     | 0.9741 | 0.9569        | 0.9063         |
| $\sigma_u$ | 126.59          | 0.0001                         | 0.1939                   | 42.7681                   | 0.9948 | 0.9869        | 0.9894         |
| $D$      | 34.41            | 0.0001                         | 0.1372                   | 18.5288                   | 0.9752 | 0.9469        | 0.9553         |

The model significant ($p$-values) are less than 0.05 for all ECAP responses, indicating that the independent parameters, as well as the individual model coefficients and interaction terms, are statistically different from zero at the 95% confidence level. The ECAP responses’ lack of fit is greater than 0.05, implying that the model is good [63]. The signal to noise (S/N) ratio is computed with “adequate precision” to determine the model’s validity. It is recommended that the ratio exceed four [62]. The ECAP responses’ adequate precision is greater than four and indicates that there is sufficient signal and the model can be applicable to navigate the design space. The regression coefficient $R^2$ is high and indicates that the ECAP responses’ model created by the experiment is desirable. The adjusted $R^2$ for the five responses is close to the predicted coefficient $R^2$.

3.3. Optimization Results

3.3.1. RSM Results

This section presented the optimal ECAP condition of the desire response. Stat-Ease Design Expert software (version 13.0.5) is a useful tool for optimizing the ECAP condition. Figure 11 shows the optimal $G_R$ response of ECAP process and corresponding conditions. For all the following optimization findings the red dot and the blue dotes the indicated the ECAP processing condition and ECAP response, respectively. The optimization target is set to “In range”, and the solution destination is set to “Minimize.” The desirability function’s predicted output is in the form of “smaller-is-better” characteristics. The optimal process condition values include number of passes (A) = 4 passes, die angle (B) = 90°, dummy variable $X_1$ (C) = 0 and dummy variable $X_2$ (D) = 1 for minimum $G_R$ value of 0.8872 $\mu$m. The optimum value of $G_R$ was obtained in the range between 0.88 and 2.62 $\mu$m.

Figure 11. Optimal ECAP process parameter of $G_R$. Red dots: ECAP condition. Blue dots: ECAP response.
In addition, the optimal $H_C$ response of ECAP process and corresponding conditions is presented in Figure 12. The optimization target is set to “In range”, and the solution destination is set to “Maximize.” The desirability function’s predicted output is in the form of “larger-is-better” characteristics. The optimal process condition values include number of passes ($A$) = 4 passes, die angle ($B$) = 90°, dummy variable $X_1(C) = 0$ and dummy variable $X_2(D) = 1$ for maximum $H_C$ value of 46.02 HV. The optimum value of $H_C$ was obtained in the range between 36 and 46.5 HV.

![Figure 12. Optimal ECAP process parameter of $H_C$. Red dots: ECAP condition. Blue dots: ECAP response.](image)

Furthermore, Figure 13 illustrates the optimal $H_E$ response of ECAP process and corresponding conditions. The optimization target is set to “In range”, and the solution destination is set to “Maximize.” The desirability function’s predicted output is in the form of “larger-is-better” characteristics. The optimal process condition values include number of passes ($A$) = 4 passes, die angle ($B$) = 90°, dummy variable $X_1(C) = 0$ and dummy variable $X_2(D) = 1$ for maximum $H_E$ value of 53.924 HV. The optimum value of $H_E$ was obtained in the range between 42 and 55 HV.

![Figure 13. Optimal ECAP process parameter of $H_E$. Red dots: ECAP condition. Blue dots: ECAP response.](image)

Figure 14 presents the optimal $\sigma_u$ response of ECAP process and corresponding conditions. The optimization target is set to “In range”, and the solution destination is set to “Maximize.” The desirability function’s predicted output is in the form of “larger-is-better” characteristics. The optimal process condition values include number of passes ($A$) = 2 passes, die angle ($B$) = 120°, dummy variable $X_1(C) = 0$ and dummy variable $X_2(D) = 1$ for maximum $\sigma_u$ value of 388 MPa. The optimum value of $\sigma_u$ was obtained in the range between 275 and 388 MPa.

![Figure 14. Optimal ECAP process parameter of $\sigma_u$. Red dots: ECAP condition. Blue dots: ECAP response.](image)

Finally, Figure 15 shows the optimal $D$ response of ECAP process and corresponding conditions. The optimization target is set to “In range”, and the solution destination is set to “Minimize.” The desirability function’s predicted output is in the form of “smaller-is-better” characteristics.
variable $X_3(C) = 0$ and dummy variable $X_2(D) = 1$ for maximum $\sigma_u$ value of 388 MPa. The optimum value of $\sigma_u$ was obtained in the range between 275 and 388 MPa.

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{figure14}
\caption{Optimal ECAP process parameter of $\sigma_u$. Red dots: ECAP condition. Blue dots: ECAP response.}
\end{figure}

Finally, Figure 15 shows the optimal $D$ response of ECAP process and corresponding conditions. The optimization target is set to “In range”, and the solution destination is set to “Minimize.” The desirability function’s predicted output is in the form of “smaller-is-better” characteristics. The optimal condition values include number of passes ($A$) = 4 passes, die angle ($B$) = 90°, dummy variable $X_1(C) = 0$ and dummy variable $X_2(D) = 1$ for minimum $D$ value of 29.0283%. The optimum value of $D$ was obtained in the range between 28 and 39.5%. For a confirmation test, these optimum conditions of ECAP and responses are compared to the GA results obtained in the next step.

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{figure15}
\caption{Optimal ECAP process parameter of $D$. Red dots: ECAP condition. Blue dots: ECAP response.}
\end{figure}

3.3.2. GA and Hybrid RSM-GA Results

Genetic algorithm (GA) used to determine the optimum set of the ECAP independent variables that contribute to the lowest possible $G_R$ and $D$, and the higher possible $H_C$, $H_E$, and $\sigma_u$. Each ECAP response proposed in Equation (3) to Equation (7) is taken as the objective function and subjected to the ECAP boundary condition, $N$, $\varphi$, $X_1$ and $X_2$ by using genetic algorithm can be expressed as:
Minimize ECAP (number of passes, ECAP die angle, $X_1$, $X_2$). Subjected to ranges of ECAP condition:

1 \leq N \leq 4 \text{ (pass)}

90 \leq \phi \leq 120 \text{ (°)}

$X_1 \in [0,1]$

$X_2 \in [0,1]$

For GA optimization technique, the performance of fitness value and run solver view results from MATLAB show the best $G_R$ and corresponding ECAP conditions. The best value of $G_R$ by GA is 0.8872 $\mu m$ obtained at four passes, 90° die angle and route Bc for $N$, $\phi$ and processing route type, respectively, as shown in Figure 16. In order to improve the results of GA, hybrid of response surface methodology and GA (RSM-GA) was performed. An initial population of hybrid RSM-GA based on RSM optimum ECAP condition of $N$, $\phi$, $X_1$ and $X_2$ are four passes, 90°, 0 and 1, respectively. The minimum optimum $G_R$ by hybrid RSM-GA is 0.8872 $\mu m$ obtained at four passes, 90° and route Bc.

The optimization of hardness response by GA is presented in Figure 17. The maximization of $H_C$ and $H_E$ proposed in Equations (4) and (5) is taken as the fitness function and subjected to the ECAP boundary condition. The best value of $H_C$ and $H_E$ by GA is 45.9927 HV and 53.9068 HV, respectively, obtained at four passes, 90° die angle and route Bc. Hybrid (RSM-GA) of $H_C$ and $H_E$ was performed to improve the results of GA. The maximum optimum $H_C$ and $H_E$ by hybrid RSM-GA are 45.9927 HV and 53.9068 HV, respectively, obtained at four passes, 90° die angle and route Bc, as shown in Figure 17.

The optimization of tensile response, $\sigma_u$ and $D$, by GA is presented in Figure 18. The maximization of $\sigma_u$ proposed in Equation (6) is taken as the fitness function and subjected to the ECAP boundary condition. The best value of $\sigma_u$ by GA is 388 MPa obtained at two passes, 120° die angle and route Bc.

On the other hand, the minimization of $D\%$ proposed in Equation (7) is taken as the fitness function and subjected to the ECAP boundary condition. The best value of $D\%$ by GA is 28.99% obtained at four passes, 90.29° die angle and route Bc. The maximum $\sigma_u$ by hybrid RSM-GA is 388 MPa obtained at two passes, 120° die angle and route Bc. Moreover, minimum optimum $D\%$ by hybrid RSM-GA is 28.899 % obtained at four passes, 90° die angle and route Bc, as shown in Figure 18. Table 5 summarized the comparison of ECAP responses values at experimental, RSM, GA and hybrid RSM-GA.
The optimization of hardness response by GA is presented in Figure 17. The maximization of HC and HE proposed in Equations (4) and (5) is taken as the fitness function and subjected to the ECAP boundary condition. The best value of HC and HE by GA is 45.9927 HV and 53.9068 HV, respectively, obtained at four passes, 90° die angle and route Bc. Hybrid (RSM-GA) of HC and HE was performed to improve the results of GA. The maximum optimum HC and HE by hybrid RSM-GA are 45.9927 HV and 53.9068 HV, respectively, obtained at four passes, 90° die angle and route Bc, as shown in Figure 17.

Table 5. Summary results of pure Mg ECAP process.

| Response | Experimental | RSM | GA | RSM-GA |
|----------|--------------|-----|----|--------|
| GR       | Value Cond.  | 0.88| 0.8872| 0.8872| 0.887287|
|          | 4passes, 90°, Route Bc | 4passes, 90°, Route Bc | 4passes, 90°, Route Bc | 4passes, 90°, Route Bc |
| HC       | Value Cond.  | 46.5| 46.02| 45.9927| 45.9927|
|          | 4passes, 90°, Route A | 4passes, 90°, Route Bc | 4passes, 90°, Route Bc | 4passes, 90°, Route Bc |
| HE       | Value Cond.  | 55  | 53.924| 53.9068| 53.9068|
|          | 4passes, 90°, Route Bc | 4passes, 90°, Route Bc | 4passes, 90°, Route Bc | 4passes, 90°, Route Bc |
| σu       | Value Cond.  | 388 | 388 | 388 | 388|
|          | 2passes, 120°, Route Bc | 2passes, 120°, Route Bc | 2passes, 120°, Route Bc | 2passes, 120°, Route Bc |
| D        | Value Cond.  | 28  | 29.0283| 28.9956| 28.899|
|          | 4passes, 90°, Route Bc | 4passes, 90°, Route Bc | 4passes, 90°, Route Bc | 4passes, 90°, Route Bc |
Figure 18. Optimum $\sigma_u$ (a,b), and D (c,d) by GA (a,c), and hybrid RSM-GA (b,d).

3.3.3. Validation of GA

This section proposed the optimal ECAP parameters of different responses, namely $G_R$, $H_C$, $H_E$, $\sigma_u$ and D. The presented optimal ECAP parameters, such as $N$, $\phi$ and processing route type, are based on previous studies of pure Mg that recommended the number of passes from one to twelve passes and ECAP die angle from $70^\circ$ to $135^\circ$ [64-67]. Table 6 presents the optimal condition of ECAP process of different responses by genetic algorithm (GA) and hybrid RSM and GA.

| Response | GA | RSM-GA |
|----------|----|--------|
| $G_R$ (\(\mu\)m) | Value | 0.269927 | 0.269927 |
| Cond. | 4passes, 70°, Route Bc | 4passes, 70°, Route Bc |
| $H_C$ (HV) | Value | 47.4951 | 47.4951 |
| Cond. | 4passes, 80°, Route Bc | 4passes, 80°, Route Bc |
| $H_E$ (HV) | Value | 54.7207 | 54.7207 |
| Cond. | 4passes, 80°, Route Bc | 4passes, 80°, Route Bc |
| $\sigma_u$ (MPa) | Value | 422.5 | 422.5 |
| Cond. | 2passes, 135°, Route Bc | 2passes, 135°, Route Bc |
| D (%) | Value | 4.0846 | 4.0846 |
| Cond. | 6passes, 80°, Route Bc | 6passes, 80°, Route Bc |
4. Conclusions

Billets of pure Mg were processed through ECAP up to four passes of routes Bc, A and C using two dies with channel angles of 90° and 120° at a temperature of 225 °C.

Many empirical models were developed to assess the effect of ECAP processing parameters on the microstructural evolution and mechanical properties of Mg billets. The following conclusions can be extracted:

1. ECAP parameters of four passes, φ = 90° and route Bc produce the most significant grain refinement.
2. 4-Bc experienced a significant reduction in the grain size by 86% compared to the as-annealed counterparts.
3. ECAP parameters of four passes, φ = 90° and route Bc resulted in the best Vicker’s microhardness values at both the central and the peripheral regions.
4. 4-Bc processing through the 90° die angle recorded a significant HV increase at the edge and central areas by 112% and 78%, respectively, compared to the as-annealed counterpart.
5. ECAP parameters of two passes, φ = 120° and route Bc resulted in the highest ultimate tensile strength.
6. ECAP parameters of four passes, φ = 90° showed the most enhancement in the ductility at fracture of the Mg billets.

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Nomenclature

| Term   | Description                           |
|--------|---------------------------------------|
| ECAP   | equal channel angular pressing         |
| RSM    | response surface methodology          |
| ANOVA  | analysis of variance                  |
| HCP    | hexagonal close-packed                |
| SPD    | severe plastic deformation            |
| UFG    | ultra-fine grain                      |
| ε_eq   | the equivalent strain                 |
| φ      | ecap die angle                        |
| Ψ      | outer corner angle                    |
| N      | number of passes                      |
| FESEM  | field emission scanning electron 
  microscope |
| EBSD  | Electron back-scatter diffraction    |
| 1P     | one pass                              |
| 4P     | four passes                           |
| AA     | as-annealed                           |
| IPF    | inverse pole figure                   |
| Hv     | vicker’s microhardness                |
CCD central composite design  
DF desirability function  
GA genetic algorithm  
FDM fused deposition modeling  
GA-ANN genetic algorithm-artificial neural network  
GA-RSM genetic algorithm-response surface methodology  
GA-ANFIS genetic algorithm-adaptive neuro fuzzy interface system  
\( G_R \) grain size  
\( H_C \) hardness measurement at center  
\( H_E \) hardness measurement at edge  
\( \sigma_u \) ultimate tensile strength  
D ductility  
\( X_1 \) and \( X_2 \) dummy variables  
\( R^2 \) regression coefficient  
S/N signal to noise

Appendix A

Table A1. Design of experiment of ECAP parameters and their response.

| Run | A | B | C | Grain Size | Hardness | Tensile Strength |
|-----|---|---|---|------------|----------|-----------------|
|     | N |  |   | \( G_R \) (µm) | \( H_E \) (HV) | \( H_C \) (HV) | \( \sigma_u \) (MPa) | D (%) |
| 1   | 1 | 2 | 120 | A | 2.62 | 42 | 36 | 278 | 33.5 |
| 2   | 2 | 2 | 120 | A | 2.33 | 46.6 | 37 | 282 | 38 |
| 3   | 4 | 90 | C | 1.22 | 51.2 | 43 | 327 | 33 |
| 4   | 2 | 120 | C | 2.46 | 45.6 | 36.4 | 280 | 38.5 |
| 5   | 2 | 90 | Bc | 1.38 | 51 | 45.5 | 320 | 36.5 |
| 6   | 2 | 120 | A | 2.38 | 46 | 37.8 | 290 | 38 |
| 7   | 2 | 90 | Bc | 1.43 | 51 | 44 | 318 | 37 |
| 8   | 4 | 120 | Bc | 1.89 | 51 | 42 | 319 | 39 |
| 9   | 4 | 120 | C | 1.99 | 50.2 | 40.5 | 315 | 39.5 |
| 10  | 2 | 120 | Bc | 2.14 | 47 | 38.5 | 388 | 37 |
| 11  | 1 | 120 | A | 2.54 | 43.2 | 36.5 | 275 | 34 |
| 12  | 4 | 90 | Bc | 0.88 | 55 | 46 | 340 | 28 |
| 13  | 1 | 90 | A | 1.95 | 48 | 39 | 308 | 38.5 |
| 14  | 4 | 90 | A | 0.98 | 52.5 | 46.5 | 330 | 31 |
| 15  | 4 | 90 | A | 1.02 | 52.8 | 44.6 | 328 | 32 |
| 16  | 1 | 90 | A | 1.86 | 46 | 40.5 | 311 | 37 |

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