**AttWalk: Attentive Cross-Walks for Deep Mesh Analysis**

Ran Ben Izhak  
Technion, Israel  
benizhakran@gmail.com

Alon Lahav  
Technion, Israel  
alon.lahav2@gmail.com

Ayellet Tal  
Technion, Israel  
ayellet@ee.technion.ac.il

![Most & least attentive walks.](image)

**Abstract**

Mesh representation by random walks has been shown to benefit deep learning. Randomness is indeed a powerful concept. However, it comes with a price—some walks might wander around non-characteristic regions of the mesh, which might be harmful to shape analysis, especially when only a few walks are utilized. We propose a novel walk-attention mechanism that leverages the fact that multiple walks are used. The key idea is that the walks may provide each other with information regarding the meaningful (attentive) features of the mesh. We utilize this mutual information to extract a single descriptor of the mesh. This differs from common attention mechanisms that use attention to improve the representation of each individual descriptor. Our approach achieves SOTA results for two basic 3D shape analysis tasks: classification and retrieval. Even a handful of walks along a mesh suffice for learning.

**1. Introduction**

Shape analysis of 3D objects is a fundamental aspect in modern computer vision and computer graphics research. This is due to the paramount importance of shape analysis to numerous applications, including self-driving cars, virtual & augmented reality, robotics, medicine and many more.

There are several representations of 3D objects, most notably triangular meshes, point clouds and volumetric data. This work focuses on triangular meshes, which are the most common representation in computer graphics, thanks to its efficiency and high-quality. However, 3D meshes are unordered and irregular, which is challenging for deep learning algorithms. This has led to attempts to "re-order" the data and re-define the convolution & pooling operations, in order to be able to utilize CNNs [14, 22, 53, 55].

Our work is inspired by a recent framework, named *Meshwalker* [31], which does not attempt to use CNNs at all. Instead, it suggests to capture the geometry & topology of a mesh by randomly walking along its surface. Each
walk is processed by a Recurrent Neural Network (RNN), aggregating surface information along the walk. Given a mesh, it is represented by several random walks, which are generated independently. Meshwalker achieves outstanding results, demonstrating the power of randomness.

In this paper, we attempt to overcome the major drawback of Meshwalker: Randomness may result in walks that do not represent the mesh well, sometimes leading to failures even when many walks are used. Our goal is to focus on portions of the walk that distinguish a mesh from others. We propose to learn how to weigh the features of the various walks. Interestingly, this yields insight regarding the distinctiveness of mesh regions. For instance, walk features related to the guitar’s neck and strings are more meaningful than those related to the guitar’s body (Figure 1).

This idea is related to the popular notion of attention, first introduced by [2] for language translation. Since then, many natural language processing (NLP) tasks, as well as image analysis tasks have used attention. The work on 3D attention, in particular on meshes, is sparser [33, 38, 61].

We propose a novel walk-attention mechanism. We exploit the fact that multiple walks along a mesh result in multiple representations of this mesh. These walks can provide information to each other on the important features of the walk and jointly derive a good description of the mesh. For intuition sake, let us draw an analogy to sentences. Suppose that we are given different sentences describing the same event (i.e., various walks describing the same mesh). Our goal is come up with a single description of the significant features of the event, by utilizing the collection of sentences. This differs from common attention units, which aim at improving the descriptors of the various sentence.

To realize this idea, we learn a novel attention map between the feature vectors representing the walks along the mesh. Rather than using the attention vectors as new feature vectors, as common, we interpret them as crosswalk probabilities. This will enable us to use them, jointly with the original feature vectors, to generate a single mesh descriptor. This descriptor focuses on the distinctive mesh features encountered by specific random walks, while neglecting the effect of commonplace features encountered by others.

Figure 1 illustrates the most attentive walks—those that influence the final mesh descriptor the most (and similarly, the least attentive walks). Indeed, the most attentive walk of the stool, as determined by our model, is one that goes both through the seat and a leg, whereas the least attentive walk goes only through the seat, and thus missing information needed for classification. Similarly, the most attentive walk of the guitar explores the neck and the strings, and that of plant explores the flowers (neglecting the walk on the vase).

In addition to achieving SOTA results, our framework is able to analyze shapes using significantly less walks for certain datasets. For instance, for Modelnet40, \(\frac{1}{5}\) of the walks suffice, compared to [31], while the results improve. This is thanks to focusing on the most distinctive portions of the walks, rather than averaging all random walks.

We evaluate our method for two fundamental shape analysis applications: mesh classification and mesh retrieval. We show that it outperforms other methods for commonly-used datasets, as well as for a challenging new dataset [16]. Hence, this paper makes a couple of contributions:

1. We introduce a novel attention mechanism to deep learning on meshes. This mechanism also provides insight as to which regions of 3D objects are more important for shape analysis tasks and which are less.

2. We present an end-to-end learning framework that realizes this attention. It achieves state-of-the-art results for 3D shape classification and retrieval, even when using significantly few walks.

2. Related work

Mesh deep learning. A triangular mesh is the most widespread 3D representation in computer graphics. A mesh is represented as a set of vertices \(V\), edges \(E\) and faces \(F\). Since each vertex has a different number of neighbors, at different distances, the basic question is how the irregular nature of this representation shall be handled, so as to suit Convolutional Neural Networks (CNNs).

In an attempt to "re-order" the data, it was suggested to convert the mesh into volumetric grids [4] or into multiple 2D projections (multi-view) [15, 50, 48, 54]. Point clouds have been handled quite intensively as well, resulting in interesting convolution and pooling operators [1, 42, 44, 51, 60]. Recently, implicit functions have also been proposed to represent 3D mesh for deep learning [17, 29, 37, 49]. See [18] for a thorough review.

To handle meshes directly, novel convolutions and/or vertex neighborhoods have been defined [14, 19, 41, 46, 53]. Other works parameterize the mesh in 2D [5, 12, 25, 30, 47]. In [22], a unique idea of using the edges of the mesh to perform pooling and convolution, is introduced.

Our work is based on yet another idea, termed MeshWalker, of representing a mesh by a set of random walks over its vertices, along the edges [31]. In a walk, each vertex is represented as its 3D offset from the previous vertex of the walk. The walk is fed into a Recurrent Neural Network (RNN) that "remembers" the walk’s history.

3D attention. Attention was first introduced by [2] for language translation and since then have revolutionized natural language processing (NLP) [8]. The success in NLP has inspired applications of attention to image analysis tasks. These include, among others, recognition [11, 26, 66], image synthesis [64], and image captioning [59, 63].

In 3D, many of the works utilize attention within the multi-view representation, either aggregating features by at-
tention in consecutive views [20, 23, 54] or, in addition, selecting the next views according to attention [7, 21]. Recently, attention has been used also for point clouds, attempting to capture the local context of a point [27, 65] or the global context [39, 50]. Others have learned contextual relation between point patches [57]. Point transformers have also been proposed [58, 62].

The work on mesh attention, however, is sparser. It was used for reconstructing 3D human pose [33], for mesh deformation [61], or for classification and segmentation [38]. In PD-Meshnet [38], the primal-dual graph framework is extended to 3D meshes, utilizing graph attention network to capture global context. The non-local nature of transformers is exploited in [33]. Attention masks are extracted in [61] in order to attend different shape parts at lower scale, enabling fine part-deformation for local attentive regions.

Our proposed attention is inherently different. It operates on multiple random walks on a mesh, using attention to learn to produce a single cross-walk attentive features.

3. Model

We wish to learn how to separate the wheat from the chaff, focusing on the relevant features of the mesh and ignoring the irrelevant ones. For instance, to distinguish a stool from a chair in Figure 1, it is useless to explore their seats; rather it is useful to identify the backrest (or the lack of it). Generally, in Figure 1 it is better to focus on the features along the cyan walk than on features along the magenta walk.

We propose a novel model that makes use of the fact that we have multiple pieces of information. In particular, we benefit from having multiple random walks, which explore the mesh in diverse manners. Briefly, a random walk is defined as a series of vertices, whose first vertex is selected randomly, and then the next vertices are added iteratively, where each vertex is chosen randomly from the vertices adjacent (along a joint edge) to the current one. Each vertex of a walk is represented as the 3D translation from the previous vertex. Thus, each walk wanders around the mesh, going through meaningful, as well as non-meaningful parts of the mesh. In MeshWalker [31], for each random walk a different feature vector is learned, describing the mesh from the specific walk’s perspective.

Our key idea is that, given multiple feature vectors, learned from their respective walks, we will learn to focus on the most informative entries of these descriptors. This is done by a novel Many-to-One (MtO) attention module that, given information from multiple sources, generates a single feature vector. This descriptor highlights the informative features and neglects the others.

In analogy to multiple sentences that describe the same event, we are given multiple walks that describe the same mesh. Each sentence is processed separately and a feature vector is generated for it, describing the event as expressed by this sentence. Our goal is to learn a single feature vector that describes the event as a whole, by utilizing the collection of feature vectors generated for the sentences. This is different from from common attention units [52], where attention is used to improve the individual descriptors. We note that this analogy is not complete, as randomness is unique to our case.

Specifically, our attention module gets as input $n$ feature vectors for $n$ walks. We may think of every vector’s entry as describing a certain property of the walk. Thus, in order to compute entry $i$ in the resulting mesh feature vector, all $i$-s entries of the walk feature vectors are used, independently of the other vectors’ entries. This is done by learning a weight for each entry of each feature vector. For learning these weights, however, all entries from all feature vectors are used. Finally, the weight vectors, jointly with the walk feature vectors, are used to generate the final result. In the following we will elaborate on the details of this idea. However, we note already that our scheme may be beneficial in other scenarios where the same object/scene/event can be described in diverse, though tightly related, manners.

Figure 2 illustrates the architecture of our proposed model. It consists of $n$ instances of MeshWalker, excluding the last classification layer. Each instance processes a single walk, $w_i$, independently, generating a feature vector for this walk $f_{w_i}$, $1 \leq i \leq n$. These feature vectors constitute the input to our cross-walk attention module, which generates a single feature vector that describes the mesh, $f_{\alpha}$. The final prediction vector, $\hat{p}$, is generated by a fully-connected layer, which gets $f_{\alpha}$ as input. Hereafter, we briefly describe MeshWalker and then elaborate on the attention module, which is the key of the framework.

MeshWalker. As illustrated in Figure 3, MeshWalker [31] gets as input the 3D coordinates of the vertices along the walk. It first learns to map each vertex to a new feature space in high dimension by fully-connected layers. Then, a Recurrent Neural Network (RNN), having a hidden state vector (“memory”) that contains the information gathered along the walk, is applied. It learns to accumulate the important information along the walk and forget the non-important information. The RNN is implemented using three Gated Recurrent Units (GRU) [9].

Cross-walk attention. Our proposed cross-walk attention block is illustrated in Figure 4. Given $n$ feature vectors of $n$ walks, the attention module learns how to aggregate the important information from all the walks, while discarding the irrelevant information. This block consists of two sub-blocks. In the first, the multiple walks are utilized in order to produce a better description for each walk separately, generating an individual attentive vector per walk. Then, these attentive vectors are put together in a way that provides a single attentive vector for the whole mesh.
Each walk, \( w_i \), is processed independently by *Meshwalker* [31], excluding its last classification layer, resulting in a feature vector, \( f_{w_i} \), for each walk. These \( n \) feature vectors are the input to our novel attention module, which produces a single mesh feature vector, \( f_a \), which emphasizes the most attentive properties of the mesh. The last fully-connected layer transforms \( f_a \) into a probability vector, which is used for shape analysis applications (e.g. \( p \) is a prediction vector for classification). Figures 3 and 4 illustrate the architectures of MeshWalker and the attention module.

**Figure 2: Architecture.** Each walk, \( w_i \), is processed independently by *Meshwalker* [31], excluding its last classification layer, resulting in a feature vector, \( f_{w_i} \), for each walk. These \( n \) feature vectors are the input to our novel attention module, which produces a single mesh feature vector, \( f_a \), which emphasizes the most attentive properties of the mesh. The last fully-connected layer transforms \( f_a \) into a probability vector, which is used for shape analysis applications (e.g. \( p \) is a prediction vector for classification). Figures 3 and 4 illustrate the architectures of MeshWalker and the attention module.

**Figure 3: Meshwalker [31].** This network gets as input a random walk (a sequence of vertices) along the mesh, \( w_i \). Each vertex is first embedded into a higher dimension feature vector by two fully-connected layers. Then, subsequent three RNN (GRU) layers process the sequence of feature vectors into a single walk feature vector, \( f_{w_i} \), which describes the properties of the walk.

In particular, for the first sub-block, we are given \( n \) walk feature vectors \( \{ f_{w_i} \}_{i=1}^n \), stacked to form a matrix \( F_{w} \). The goal is to generate a new matrix of walk features, \( H_a \), in which each walk is enriched by information from other walks. Given \( F_{w} \), we learn its self-attention map, using the scaled dot-product attention block of [32], which transforms each walk features into a self-attention vector. Briefly, \( F_{w} \) is transformed into three feature sub-spaces \( Q, K, V \). Intuitively, the columns of \( Q \) and \( K \) are walks descriptors, learned to represent relevancy to one another. While \( Q \) and \( K \) play a similar role, their different walk descriptors enable the walks to influence one another in a non-symmetric manner. \( V \)’s columns represent intra-walk attention per entry. \( Q, K, V \) are computed as follows:

\[
Q = W^{(q)} F_{w}, \quad K = W^{(k)} F_{w}, \quad V = W^{(v)} F_{w}, \tag{1}
\]

where \( W^{(q)}, W^{(k)}, W^{(v)} \in \mathbb{R}^{d \times d} \) are learned weight matrices that are used to project the walk feature vectors into different sub-spaces of dimension \( d \) (in our implementation \( d = 512 \), the same dimension as that of the walk feature vectors). The self-attention weights are computed as

\[
W_{sa} = \text{softmax} \left( \frac{QK^T}{\sqrt{d}} \right). \tag{2}
\]

Finally, the self-attention feature vectors are aggregated in matrix \( H_a \). Each column of \( H_a \) utilizes knowledge from all the walks and will be used next to weigh the importance of the different features of each walk, in order to represent the mesh as a whole. \( H_a \) is defined as

\[
H_a = W_{sa} V. \tag{3}
\]

The second sub-block (the cross-walk attention sub-block in Figure 4) aims at aggregating the walk features in \( F_{w} \) into a single mesh feature vector \( f_a \). This is done by utilizing \( H_a \), in which each entry indicates the importance of that entry. \( H_a \) is first given a probabilistic interpretation, by applying softmax per row \( i \). These probabilities are then multiplied, element-wise, by the walk feature vectors \( F_{w} \), to create cross-walk attention features. That is to say, every
both phases can be trained by the same loss. Given a pre-

Training. Our model is trained in two phases. At first, the cross-walk attentive features seamlessly. This is essential to the model learn to extract meaningful features for each walk, attempting to correctly classify the shape by every single walk. This assists in extracting the best features per walk. In the second phase, we freeze the Mesh-Walker block (the cyan rectangles in Figure 2) and train the attention block, so as to account for the most relevant features across all walks. The two-phase training prevents the network from focusing only on the most attentive walks, which would result in avoiding to process mesh regions that are less attentive, but may be important for fine results. In Section 5 we compare this strategy to 1-phase training.

Recall that both the individual walk features $f_w$, and the mesh feature vector $f_a$ reside in the same sub-space, thus both phases can be trained by the same loss. Given a prediction vector (either per-walk in Phase 1 or $p$ of Figure 2 in Phase 2) and the corresponding class label $l$, for mesh classification, training is performed by minimizing the Softmax cross entropy loss

$$L(p, l) = -\log \frac{e^{p_l}}{\sum_{c=1}^{C} e^{p_c}}.$$  

For retrieval, we train our model using a combination of the softmax cross entropy loss and the triplet-center loss (TCL). Intuitively, TCL attempts to push each walk prediction vector closer to its corresponding class center and away from centers of other classes. Specifically, given $p$ and $l$ as above, the TCL is defined as

$$TCL(p, l) = \max \left(D(p, c_l) + m - \min_{k \neq l} D(p, c_k), 0 \right).$$

Here, each class is represented by a learned parametric center $c_k$ (of the same dimension as $p$). The margin $m$ is a hyper parameter that prevents pushing the vector too far ($m = 1$ in our experiments). $D(\cdot)$ is the squared Euclidean distance. The combination of the losses is defined as

$$\mathcal{L}(p, l) = \lambda_1 TCL(p, l) + \lambda_2 L(p, l).$$

In all our experiments $\lambda_1 = 1$ and $\lambda_2 = 0.01$. We note that though this loss encourages the network to learn more discriminative mesh features and indeed improves retrieval results, empirically it does not improve classification results.

In practice, training is performed in batches of $M = 64$ walks, where a batch contains walks from several meshes. In the first phase each walk belongs to a different mesh,
whereas in the second phase we use 8 walks per mesh, for 8 meshes. All the meshes in our experiments are first simplified into $1K$, $2K$ and $4K$ faces, both to reduce the network capacity required for training and as a form of data augmentation. At inference, we average the scores of the predictions at the different scales. Meshes with less faces than the above scales are used without simplification. The models are normalized into a unit cube. For our first training phase, we use Adam optimizer with cyclic learning rate of $5 \cdot 10^{-4}$ to $10^{-6}$ with $20K$ iterations per cycle, for a total of $200K$ iterations. In the second phase, we reduce the learning rate by half, which is more stable for fine-tuning the cross-walk attention block, training for additional $100K$ iterations.

4. Applications

The performance of our model is evaluated in 3D shape classification and retrieval, on a variety of datasets. For each dataset, we compare our results to the reported results; hence, each table shows results of different algorithms.

4.1. Mesh classification

Given a mesh, the goal is to classify it into one of pre-defined classes. For each mesh, we apply our model, as described in Section 4, where the last fully-connected layer outputs a classification prediction vector $p$. The three datasets utilized differ in the number of classes and the number of objects per class. We report both on instance accuracy and on class accuracy. Instance accuracy is defined as the percentage of the correctly-classified objects. Class accuracy is defined as the mean of class instance accuracy; thus it considers all classes equally, ignoring their size. The two metrics are the same for SHREC11, which is class-balanced, and differ for the imbalanced datasets, ModelNet40 & 3D-FUTURE.

3D-FUTURE [16]. This new dataset contains 9,992 industrial CAD models of furniture [15]. It consists of 7 super-categories, having 1-12 sub-categories each, for a total of 34 categories. The train/test split is 6,699/3,293. This dataset is challenging both due to the objects it contains and due to its hierarchical structure, as objects in related sub-categories may resemble each other, requiring fine-grain classification.

For this dataset, we trained our model with the class-balanced loss of [10], which was found empirically to outperform cross-entropy. This loss handles well heavily-unbalanced datasets (the number of training shapes per category ranges between 8 to 633). It is given by:

$$CB_{softmax}(p, l) = - \frac{1 - \beta}{1 - \beta^{n_l}} \log \left( \frac{e^{p_l}}{\sum_{j=1}^{C} e^{p_j}} \right).$$

For each mesh prediction vector $p$ and label $l$, we weigh the cross entropy loss according to the number of training objects with the same label $n_l$, where $\beta$ is a hyper-parameter in the range $[0, 1]$, set empirically to 0.9.

Table 1 shows that our method outperforms previous methods, both point-based or multi-view. Following [16], we omit categories with less than 10 training samples from the train/test sets, thus left with 32 categories.

SHREC11 [32]. This dataset consists of 30 classes, each contains 20 meshes. Typical classes are camels, cats, glasses, centaurs, hands etc. Following the setup of [12], the objects in each class are split into 16 (/10) training examples and 4 (/10) testing examples.

Table 2 compares the performance of state-of-the-art algorithms on this dataset. Each result is the average of 3 random splits into train/test sets. Our method outperforms SOTA methods. In fact, for the 16/4 split it achieves a perfect score and for the 10/10 split an almost-perfect score.

ModelNet40 [56]. This dataset contains 12,311 CAD models from 40 categories, out of which 9,843 models are used for training and 2,468 for testing. This dataset contains many non-watertight and multiple-component objects, which might be difficult for some mesh-based methods.

Table 3 shows that our method outperforms other mesh-based methods. We note that while in [31], 64 walks are used, in our framework 8 walks per shape suffice. This is thanks to our cross-walk attention that focuses on the relevant information from each walk and neglects the non-informative features. Our results are still not as good as those of multi-view methods. This is due to relying, in ad-

| Method          | Input       | Class  | Instance |
|-----------------|-------------|--------|----------|
| AttWalk (Ours)  | mesh        | 72.1\% | 73.7\%   |
| PointNet++ [44] | point cloud | 69.9\% | -        |
| MVCNN [48]      | multi-views | 69.2\% | -        |

Table 1: 3D-FUTURE classification (class/instance accuracy). Our results outperform those reported in [16].

| Method          | Input       | Split-16 | Split-10 |
|-----------------|-------------|----------|----------|
| AttWalk (Ours)  | Mesh        | 100\%    | 99.7\%   |
| PD-MeshNet [38] | Mesh        | 99.7\%   | 99.1\%   |
| MeshWalker [31] | Mesh        | 98.6\%   | 97.1\%   |
| HSN [55]        | Mesh        | -        | 96.1\%   |
| MeshCNN [22]    | Mesh        | 98.6\%   | 91.0\%   |
| GWCNN [12]      | Mesh        | 96.6\%   | 90.3\%   |
| SG [6]          | Mesh        | 70.8\%   | 62.6\%   |

Table 2: SHREC11 classification. Split-16/10) indicates that 16/10 objects were used for training out of 20 in each class. Our method achieves perfect results for the 16/4 split and almost perfect results for the 10/10 split.
### 4.2. Retrieval

Given a query object, the goal is to retrieve objects from a given dataset, ordered by their relevancy to the query. Relevancy is determined for each returned object according to the query’s category and sub-category (if it exists). We evaluate our method on two large-scale retrieval datasets: ModelNet40 and ShapeNet-Core55. The most common evaluation measure is the mean average precision (mAP), which is used almost solely for ModelNet40. For ShapeNet-Core55, other measures are utilized as well, most notably the Normalized Discounted Cumulative Gain (NDCG). Specifically, for a returned list with $N$ objects, we consider those that belong to the query’s category as positives and the others as negatives. mAP is the mean of the precision scores at every positive retrieved object position in the list. For NDCG, the relevancy of each returned object is graded between 0 to 3, considering both category and sub-category [23]. In [45], both macro and micro average results are evaluated. The macro-average gives equal weights to the scores of all the queries; the micro-average first averages the scores of each category and then averages the scores of the categories, giving every category an equal weight, regardless of its size.

**ModelNet40** [56]. We use the most common 9,843/2,468 train/test split (a few papers use other splits). Table 3 shows that our method achieves SOTA results.

**ShapeNet-Core55**. This dataset, which is a subset of ShapeNet, contains 51,162 3D objects from 55 categories, each is subdivided into 1 to 28 sub-categories. The dataset is split into 35,764 / 5,133 / 10,265 training / validation / testing objects. The results are reported on the test set, using the evaluation code provided by [45]. As in [45], we retrieve up to 1000 object whose Euclidean distance from the prediction vector of the query object is smaller than $2m$, where $m$ is the margin hyperparameter from Equation 7.

Table 5 shows that the performance of our method outperforms those of state-of-the-art methods in both metrics. Recall that NDCG takes into account the sub-categories, thus our high scores demonstrate how well our cross-walk attention captures the objects’ distinctive features. This property can also be observed in Figure 1. The bathtub and the desk are erroneously classified by [31] as a lamp and a sink, respectively. Our method correctly focuses on walks that depict a broader view of the objects, including their outlines, resulting in correct classification.

### 5. Ablation Study

**Insights on the most/least attentive walks.** What characterizes attentive walks? To answer this question we analyze the results of ModelNet40 classification. We consider the attention rank of a walk according to its contribution to the final mesh feature vector $F_a$. Since the contribution of a walk to each entry of $F_a$ differs, we average these contributions. Hereafter we discuss the affects we studied.
(1) All walks contribute to the final feature vector, however the contribution of the most attentive walk is 70% higher than that of the least attentive walk (17% vs. 10%).

(2) The most-attentive walk is 36% longer than the least attentive walk on average. A possible explanation is that longer edges tend to describe the outline of the object, which is meaningful for capturing the shape of the object.

(3) No correlation is found between the number of faces adjacent to the walk and the attentiveness of the walk. However, similarly to (2), the most attentive walks "cover" more surface area (of the faces adjacent to the walk).

(4) The median Gaussian curvature of the most attentive walk is smaller (by 21%) than that of the least attentive walk. This can be explained, similarly to (2), by the fact that attentive walks tend to describe the major parts of the object and not to focus on small (high-curvature) details.

**Training: 2-phase vs. 1-phase.** Recall that we train our model in two phases, first training only MeshWalker and then training only the attention module. We compare this procedure to a single-phase (end-to-end) training, for ModelNet40 and 3D-Future. For both datasets, 2-phase training yields better results: The instance accuracy is 92.5 vs. 89.2 for ModelNet40 and 73.7 vs. 71.4 for 3D-Future. A possible explanation is that 2-phase training forces MeshWalker to learn the most meaningful features for each walk independently, whereas an end-to-end system makes it easier to focus on the "easier" (more meaningful) walks. As we saw above, even the least-attentive walks contribute to the final results, and hence should not be neglected.

**Number of walks.** How many random walks suffice for optimal exploration of a mesh? Table 6 shows that 8 walks already achieve the best results for SHREC11 classification. Similar results are shown in Table 3 for ModelNet40.

| # Walks | 1  | 2  | 4  | 8  | 16 | 32 |
|---------|----|----|----|----|----|----|
| Accuracy| 98.1 | 99.1 | 99.6 | 99.7 | 99.7 | 99.7 |

Table 6: **Number of walks.** 8 walks suffice for best performance, in contrast to 32 walks used.

**Alternative walk aggregation methods.** Our model aggregates walks using our novel attention scheme. Table 7 compares our results to alternative aggregation strategies for generating a single shape descriptor from multiple walk features. It shows that our proposed scheme outperforms average & max pooling on \( f_w \), as well as adding average & max pooling to the self-attention matrix \( H_a \). The latter two aggregations demonstrate that indeed self-attention by itself does not suffice for achieving SOTA results.

| Aggregation method     | Class | Instance |
|------------------------|-------|----------|
| Cross-walk Attention (our) | 72.1  | 73.7     |
| Average pooling         | 70.1  | 71.0     |
| Max pooling             | 58.2  | 60.5     |
| \( H_a + \) Average pooling | 69.3  | 71.7     |
| \( H_a + \) Max pooling  | 69.7  | 71.3     |

Table 7: **Walk aggregation methods.** Our attention approach outperforms other possible aggregation strategies on 3D-Future.

SHREC11, we get 90.5 accuracy when the walk contains 0.1 of the vertices, 99.2 accuracy for 0.2 of the vertices, and 99.7 accuracy for 0.3 or more of the vertices.

**Limitations.** Figure 5 illustrates a failure case, where a majority rule of \([31]\) would be preferable. Though 5 of 8 walks indicate that the shape is a bathtub, our attention gives more weight to features that indicate that this is a bed. The most attentive walk (in cyan), which provides a global view of the shape, classifies it as a bed due to the special shape of this bathtub. The least attentive walk (in magenta) visits mostly the tap and thus classifies the bathtub as a sink.

![Figure 5: Limitation. Our algorithm classifies the bathtub as a bed, giving more attention to features resembling a bed, as shown by the most attentive walk (in cyan).](image)

6. **Conclusion**

This paper introduced attention into a 3D learning framework. It showed how multiple random walks along the surface may jointly indicate the most attentive features of a 3D mesh. The key idea is that exploring the mesh in different ways, by different walks, can be leveraged for both learning the meaningful attributes of the surface and to reduce the number of walks needed. Our approach achieves state-of-the-art results for shape classification and shape retrieval on commonly-used datasets.

In the future, we intend to adapt our approach to other applications, most notably shape segmentation. Using our approach within multi-scale is also a direction that worth further studying.
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