Singling out the effect of quenched disorder in the phase diagram of cuprates

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Received 12 November 2018, revised 31 January 2019
Accepted for publication 7 February 2019
Published 7 March 2019

Abstract
We investigate the specific influence of structural disorder on the suppression of antiferromagnetic order and on the emergence of cuprate superconductivity. We single out pure disorder, by focusing on a series of $Y_{1-z}Eu_zBa_2Cu_3O_{6+y}$ samples at fixed oxygen content $y = 0.35$, in the range $0 \leq z \leq 1$. The gradual Y/Eu isovalent substitution smoothly drives the system through the Mott-insulator to superconductor transition from a full antiferromagnet with Néel transition $T_N = 320$ K at $z = 0$ to a bulk superconductor with superconducting critical temperature $T_c = 18$ K at $z = 1$, $YBa_2Cu_3O_{6.35}$. The electronic properties are finely tuned by gradual lattice deformations induced by the different cationic radii of the two lanthanides, inducing a continuous change of the basal Cu(1)-O chain length, as well as a controlled amount of disorder in the active Cu(2)O$_2$ bilayers. We check that internal charge transfer from the basal to the active plane is entirely responsible for the doping of the latter and we show that superconductivity emerges with orthorhombicity. By comparing transition temperatures with those of the isoelectronic clean system we determine the influence of pure structural disorder connected with the Y/Eu alloy.

Keywords: cuprate superconductors, 2D magnetism, disorder

(Some figures may appear in colour only in the online journal)
in a basal buffer layer, containing fragments of Cu(1)O chains (hereafter, chains), whereas magnetism and superconductivity take place in more distant Cu(2)O2 bilayers (hereafter planes).

Theoretically, disorder was addressed explicitly by Alvarez et al. [2], in a phenomenological model of itinerant electrons on a Cu(2)O2 square lattice showing that disorder does not lead to a universal behavior. For instance towards the clean limit, as in YBa2Cu3O6+y, it may give rise e.g. to coexistence of AF and superconducting order [3], or to an instability against charge density waves formation [4, 5], whereas quenched disorder opens a hole-density window where none of the two competing orders dominates, both having robust short range correlations. A review by Dagotto [6] highlighted that complex behaviour may emerge, leveraging on the many available degrees of freedom. Several of these considerations are in agreement with experimental results [3, 7]. However it is experimentally difficult to determine independently the effect of doping and quenched disorder [1], since they are strictly proportional to one another in all quoted examples. Only Y1−xCa1-xBa2-x2Cu3O6+y, to date, allowed this distinction [8–10], thanks to its double doping channel.

The connection between doping and disorder is drastically altered in YEu1−x−0.23Ba2−xCu3O6+y, at constant oxygen content y, where Y3+ is randomly replaced by the isovalent Eu3+ cation with a larger radius. The stronger quenched disorder due to nearest neighbor heterovalent cations is absent, leaving only a residual, weakest quenched disorder. However, the distinct cationic radii of Y (101.9 pm) and Eu (106.6 pm) [11] very strongly affect the internal chemical doping from the buffer to the active layers: YBa2Cu3O6+y and EuBa2Cu3O6+y have very different onset thresholds for superconductivity [12] (y > 0.40 for Eu and y < 0.30 for Y), hence a narrow range of y exists for which EuBa2Cu3O6+y is still a CT insulating antiferromagnet, whilst YBa2Cu3O6+y is a bulk superconductor, despite their nominally equal total cationic charge. This is a well known fact that was never explicitly exploited until now. The strong influence of the Y/Eu steric hindrance on electronic properties was convincingly attributed by nuclear quadrupole resonance (NQR) studies [12] to the reduction of the average length ℓ of the chain fragments. The chain length in turns determines the cation ratio Cu(1)2+/Cu(1)2+ in the basal layer, hence the doping of the planes. These conclusions are supported by our density functional theory (DFT) computations for a few relevant stoichiometries.

Here, choosing y = 0.35, we show by susceptibility and muon spin spectroscopy (μSR) measurements that YEu1−x−0.23Ba2−xCu3O6+y spans the whole phase diagram, from a nearly optimal AF Néel state (with TN = 320(15) K, k = (1, 1, 0) and staggered spin basis along c in the bilayer) to a bulk underdoped superconductor with Tc = 20(2) K. This means that the electronic properties of the planes are very effectively modulated from those of a charge transfer insulator, across the metal insulator transition, by a mere structural distortion, without altering the total charge content. We show that the plane hole doping is determined by internal charge transfer, modulated by the Cu(1)O chain fragment length.

Although the isoelectronic cation substitution has no influence on the total charge content, it introduces a form of quenched disorder, absent in the end members, z = 0 and z = 1, and maximal for z = 0.5. We take advantage of the remarkably wide modulation of electronic properties brought about by the Y/Eu substitution to highlight the net effect of the well characterized quenched disorder on the native clean limit cuprate. By carefully calibrating the active layer hole content by several independent experiments, based on the Seebeck effect [13–17], on the μSR internal fields in the AF phase [17], and on the 63Cu NQR measurement of chain length, we determine quantitatively controlled disorder, plane hole doping and their joint influence on the electronic properties. This is crucial to determine the plane hole number h(z) (per square Cu(2)O2), one of the two natural independent variables, together with the standard deviation σ(z) for quenched disorder, against which we wish to assess the dependence of the electronic properties. By comparison with clean limit YBa2Cu3O6+y, this provides the pure effect of quenched disorder in a crucial region of the phase diagram.

The paper is organized as follows: in section 1 we describe the Y/Eu1−x−Ba2−xCu3O6+y sample preparation, their XRD resistivity and Seebeck characterization which provides the hole count in the z = 1 compound; section 2 reports DFT calculations and their main conclusions; susceptibility and μSR measurements are presented in section 3, with the description of strongly-underdoped YBa2Cu3O6+y hole count from μSR data; section 4 reports our NQR measurements, providing a determination of the average chain length, ℓ(z), and draws our conclusions on an absolute calibration of the hole count versus z; section 5 contains the main results, the phase diagram for YEu1−x−Ba2−xCu3O6+y, quantifying the reduction in the ordering temperatures by structural disorder.

1. Sample preparation and characterization

A series of YEu1−x−Ba2−xCu3O6+y polycrystalline samples with increasing Yttrium content z = 0.0, 0.15, 0.23, 0.3, 0.4, 0.6, 0.8 and 1.0 was prepared by the standard solid state reaction technique. The final oxygen content of the samples, y = 0.35(2), was achieved following a topoactitic–like low temperature annealing [18, 19] of stoichiometric quantities of fully oxidized and fully reduced specimens (y = 0.98(2) and y = 0.05(2), respectively), tightly packed in vessels sealed in vacuum. The low temperature annealing allows the diffusion of the mobile species O(1) inside the material towards the minimum energy configuration. The produced samples are thus chemically homogeneous, and the effective oxygen content was checked by thermogravimetry on each sample. Furthermore this procedure was shown to produce maximum length chain fragments at each composition and reproducible y dependence of the electronic properties, coinciding [17] with state of the art single crystal data [20].

1.1. Crystal structure

X-ray diffraction (XRD) patterns were collected by using a Thermo Electron ARL X’tra powder diffractometer with Cu Kα radiation equipped with a Si(Li) solid state detector allowing to eliminate the incoherent contribution produced by
the fluorescence of Eu. Data collections were performed with a step size of 0.03 degrees and a counting time of 2 s per step.

Synchrotron x-ray diffraction data were collected for the samples with $z = 0.20, 0.40, 0.85, 1$ on the ID15 beamline at the ESRF in Grenoble (France) by a Perkin-Elmer 2D CCD detector. The incident beam wavelength was set to 0.1423 Å and the 2D images with 0.0083 degree per pixel were integrated by using the FIT2D software [21] after instrumental parameters calibration with standard Ce2O3. LeBail fit of the patterns was carried out by using the GSAS software [22] with EXPGUI interface [23].

We collected powder x-ray diffraction data for all the samples presented in this work. The evolution of a selected range of the diffraction patterns is reported in figure 1, clearly showing the splitting of the 200/020 reflection of the tetragonal cell for Y content higher than 50%. Relevant microstructural effects giving rise in all cases to both asymmetric and hkl-dependent broadening of the peaks were detected, making the refinement of all the structural parameters through Rietveld analysis complex.

Therefore, a thorough study of the lattice parameters as a function of the yttrium content was performed by LeBail fitting of the patterns. Two structural models, tetragonal (T) $P4/mmm$ and orthorhombic (O) $Pmmm$, corresponding to the two end members of the series, $z = 0, 1$, respectively, were used to fit the data.

Figure 2 displays the evolution of the lattice parameters and of the cell volume with $z$ (Y content), as determined by synchrotron and home based XRD. The linear scaling of both the cell volume and $c = (a + b)/2$ with $z$ is in agreement with the Vegard law, confirming the proper Eu/Y solubility throughout the full compositional range. The occurrence of the T-O phase transition at $z_c = 0.5 \pm 0.09$ indicates that the probability of chain formation vanishes along $a$ and becomes unitary along $b$ for $z < z_c$, whereas both probabilities are equal to 0.5 for $z < z_c$.

1.2. Transport properties, hole delocalization and quenched disorder

In order to discuss the influence of quenched disorder on the electronic properties of our $Y_{1-x}Eu_xBa_2Cu_3O_6.35$ samples two key parameters are required: the carrier number $h$ per formula unit, per active Cu(2)O$_2$ layer, and an appropriate quantification of the degree of disorder.

Let us start from the hole carrier number. Stoichiometry imposes that extra holes exist, transferred from core charges of nominal valence cations to other bands, mostly in the plane or in the chain layer. In $YBa_2Cu_3O_{6+y}$ band calculations [24, 25] predict a conductive band on the Cu(1)O$_y$ sublattice for infinite long chains, consistent with experimental results for high oxygen doping $y > 0.8$, where long chain lengths are expected [26]. It is therefore safe to assume that in the Y compounds, for the present low $y$ values, $h$ accounts for all delocalized charges (with vanishing chain contribution).

Resistivity $\rho(T)$ measurements, performed by the standard four point technique on $2 \times 2 \times 14$ mm$^3$ sintered specimens are shown in figure 3 for three specific samples: the end members $YBa_2Cu_3O_{6.35}$ and $EuBa_2Cu_3O_{6.35}$ of the present series, plus a $YBa_2Cu_3O_{6.23}$ specimen (the same as in [3, 17, 27]), chosen to have the same $T_N \approx 320$ K as the first (Y) sample. The first and the last (Y) samples display insulating and superconducting properties respectively. The Eu sample lies in between, still presenting insulating character down to
electric behavior, despite their very similar properties and two with different oxygen content but the same $T_N = 320$ K.

50 K, $\text{YBa}_2\text{Cu}_3\text{O}_{6.23}$ and $\text{EuBa}_2\text{Cu}_3\text{O}_{6.35}$ show rather different electric behavior, despite their very similar $T_N$ values. This indicates that for the Eu sample a fraction of mobile holes are present outside the planes already at this low oxygen content.

Our data indicate that for this compound some conducting properties are associated with the disordered Cu(1)O$_z$ layer and the average of all lattice constants for $y = 0.35$ but different electronic properties and two with different oxygen content but the same $T_N = 320$ K.

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The room temperature Seebeck coefficient $S$ was demonstrated [13–17] to be rescalable to $h$ for the $\text{YBa}_2\text{Cu}_3\text{O}_{6+y}$ case. In a previous work [16] we accurately calibrated the exponential dependence of $S$ on the mobile holes and we further showed [17] the good agreement with an independent calibration from the $c$ lattice parameter [20] on oxygen doped $\text{YBa}_2\text{Cu}_3\text{O}_{6+y}$ single crystals. In sharp contrast with the wide modulation of electronic properties the Seebeck data for $\text{Y}_x\text{Eu}_{1-x}\text{Ba}_2\text{Cu}_3\text{O}_{6+y}$, shown in table 1, line up around two values, with a sharp jump around $z_c$, i.e. at the T-O phase transition. This may be understood assuming that the Seebeck coefficient is determined by all mobile charges and with coefficients strongly sensitive to crystal structure. In other words our empirical Seebeck calibration [16] is strictly valid only for the Y end member, but it cannot be used to measure the plane hole number $h$ for $z < 1$.

In order to determine the $z$ dependent additional contribution to mobile holes from the buffer layer we set up a formula unit calculation, that ignores band details, distinguishing only between $h$, and the remaining holes nominally assigned to the buffer layer. We assume a linear relation between $y$ content $z$ and the average Cu(1) ion charge $1 + \lambda_0 + \lambda_1 z$, to yield

$$Q_{\text{tot}} = 2h(z) + \lambda_0 + \lambda_1 z - 2y = 0. \tag{1}$$

At fixed $y$ this linear relation may by understood in terms of a transfer function proportional to the distortion introduced by the larger cation, linear in $z$ according to the XRD data of figure 2. Transfer is also proportional to the average chain fragment length, assuming a narrow distribution. This assumption will be discussed and justified in section 4 where we present the NQR derivation of the chain length dependence on $z$.

For $y = 0.35$ we rely on the Seebeck calibration of the $z = 1$ end member, $h_1 = 0.0700(25)$, to constrain equation (1), obtaining $\lambda_0 = 0.56$. Another calibration is required in the AF region and it is provided by the $\mu$SR data of section 3, and discussed in section 4.2.

Let us finally quantify quenched disorder. The agreement of the XRD data with the Vegard law indicates ideal randomness of the Y/Eu sublattice. The probability that a site is occupied by Eu is $z$, hence in a Poisson distribution its variance, $\sigma^2 = z(1 - z)$, provides an ideal case measure of quenched cation disorder.

2. Ab initio calculations on structure and magnetism

To clarify the relation between crystal structure, local structure and electronic properties, we conducted a DFT investigation of four selected Y-Eu ratios at the oxygen composition $y = 0.325 \approx 1/3$ that best approximates the experimental conditions. (We use the VASP code [28] and GGA+U with the same technicalities as in [25], in particular U is tuned to get the correct gap in the undoped end member.)

The calculations reproduce several experimental features, notably the evolution of crystal structure and ordering with composition, the approximate location of the structural phase transition, and of the hole content in the Cu planes. Figure 4 displays the energy difference of infinite-chain and broken-chain structures (represented by the oxygen configurations in the basal plane in the inset) versus composition. The main result (aside from the small difference between paramagnetic and antiferromagnetic) is a clear energy gain for the broken-chain configuration at the Eu end, that smoothly decays to a vanishing gain at the Y end. This result backs up our understanding that the chain length (hence its influence) vary smoothly in this system. In figure 5 we report the calculated values of $a$, $b$, $c$, and the average of all lattice constants for $z = 0, 0.25, 0.75, 1$. The results are quite in line with experiment: the cell-volume reduction is well reproduced; the $c$-axis length may indeed be weakly plateauing at intermediate Y concentrations; importantly, a T-O phase transition is predicted somewhere around 50% Y content.

We now make contact with the expectation that magnetism should disappear (albeit progressively, and not entirely) across the superconducting transition at $z_c \sim 0.5$, with the AF

1.0 0.8 0.6 0.4

| $z$ | $S$ | $h_{\text{int}}$ | $\sigma$ | $h$ |
|-----|-----|-----------------|--------|-----|
| 1.0 | 82  | 0.071(2)        | 0.23   | 0.052(2) |
| 0.8 | 82  | 0.071(3)        | 0.23   | 0.045(2) |
| 0.6 | 91  | 0.067(2)        | 0.15   | 0.045(3) |
| 0.4 | 157 | 0.045(2)        | 0.0     | 0.049(3) |

Table 1. Seebeck coefficient $S$ in $\mu$V/K for $\text{Y}_x\text{Eu}_{1-x}\text{Ba}_2\text{Cu}_3\text{O}_{6+y}$ and derived hole content, $h_{\text{int}}$, using the $\text{YBa}_2\text{Cu}_3\text{O}_{6+y}$ calibration of [16].
ordered and insulating state giving way to a metallic, zero-moment state. The intra-plane and inter-plane first-neighbor Cu–Cu magnetic couplings versus Y concentration, extracted from the energies of various magnetic states (ferromagnetic, AF-G, AF-A) of the Cu sublattice, are shown in figure 6 to be roughly constant versus composition and structure (they are also negative, indicating that AF-G is the most stable of the non-zero-moment structures). Clearly this means that $T_N$ would not change if the Cu moments remained unchanged throughout the series; put differently, AF-G will not disorder towards a moments paramagnet. What will happen instead is that a zero-moment paramagnet (PM) takes over at some concentration (as it does [24, 25] in YBa$_2$Cu$_3$O$_{6+y}$ around $y = 0.3$). Indeed, the energetics shows that the PM state is favored over the AF at $z = 1$ (YBa$_2$Cu$_3$O$_{6+y}$) and viceversa the AF is favored over the PM at $z = 0$ (EuBa$_2$Cu$_3$O$_{6+y}$).

In this picture, magnetic order weakens, and eventually disappears, due to the progressive reduction, and eventual extinction, of Cu moments. Previous work [24, 25] (see in particular figure 14 of [25]) suggested that this occurrence, and the prevalence of the PM over the AF, correlates with increased hole transfer from the chains to the planes: specifically, the AF state transfers less holes to the planes than the paramagnetic zero-moments state. Indeed, population analysis in the in-plane Cu $d$ states in the present case of Y substitution shows again that a lower amount of holes is transferred to the plane in the Eu-rich than in the Y-rich limit, the maximum difference between end compositions being of order 0.04/Cu. This compares well with the measured (or modeled) concentration change of mobile in-plane holes of section 4.2. While correlation is not causation, this is circumstantial evidence that the hole transfer produced by Y substitution is key to the transition from the AF insulating state to a metallic non-magnetic state.

3. The electronic state: superconducting and magnetic properties

3.1. Susceptibility

Susceptibility was determined by measuring the sample magnetization in a field of $H = 0.2$ mT in a MPMS system by quantum design superconducting quantum interference device (SQUID). Figure 7 shows the bulk zero-field-cooling low temperature magnetic susceptibility of selected samples. A linear fit may be imposed on the 90%–10% susceptibility drop, and we determine $T_c$ as the temperature where this line intercepts zero. No traces of superconductivity have been detected up to $z = 0.4$ (green triangles). A tiny diamagnetic shielding appears for $z = 0.6$ (blue diamonds), becoming more robust for higher $z$ (higher Y content).
The asymmetry is fitted to the function $A(t) = A_0 e^{-(\sigma_n^2 t^2)/2}$ where $\sigma_n \approx 0.2 \mu s^{-1}$ is the low static relaxation rate arising from the very much smaller neighboring nuclear moments.

Figures 8(d) and (e) display the temperature evolution of a representative set of Eu/Y compositions of the magnetic volume fraction $v_m(T)$ and the mean field $B_i(T)$, proportional to the staggered magnetization [17]. The Néel transition follows a narrow Gaussian distribution, its mean being the temperature where $v_m(T_N) = 0.5$, very close to where $B_i$ vanishes. For $z = 0.4$ and 0.6 the magnetic transitions temperatures are 40(20) K and 20(3) K respectively. Therefore in the range $0.4 < 1 - z < 0.6$ the very sharp drop of $T_N(h)$ flattens abruptly, turning into the low spin freezing temperature $T_f$ characteristic of the cluster spin glass state [29], in close analogy with La$_{2-x}$Sr$_x$CuO$_4$ and Y$_{1-x}$Ca$_x$Ba$_2$Cu$_3$O$_{6+y}$.

Therefore SQUID susceptometry and $\mu$SR provide clear evidence that indeed Y$_2$Eu$_{1-z}$Ba$_2$Cu$_3$O$_{6+y}$ spans a wide portion of the typical cuprate phase diagram, displaying a clear deviation from the carefully characterized behavior [17] of clean YBa$_2$Cu$_3$O$_{6+y}$, in that it shows an intermediate region of where neither the long range AF state nor the superconducting state are detected. This is the hallmark of quenched disorder [2, 6].

In the following we assume that the Néel temperature $T_N(z)$ and the local field $B_i(z, T)$ are largely insensitive to the rare earth at the Y site, as it is the case in the related system Ca$_{1-x}$La$_x$Ba$_2$Cu$_3$O$_{6+y}$ [30].

The intermediate temperature in each panel of figures 8(a)–(c) shows data just below $T_N$, characterized by overdamped precessions and increased value of the longitudinal fraction $f_L$. At the highest temperatures, well above the magnetic transition, samples are fully in the paramagnetic state and

\begin{equation}
A(t) = A_0 \left[ \sum_i f_{T,i} e^{-(\sigma_i t^2)/2} \cos 2\pi \gamma B_i t + f_L e^{-\lambda t} \right],
\end{equation}

where $\gamma = 135.5$ MHz T$^{-1}$ is the muon gyromagnetic ratio. The transverse and longitudinal muon weights $f_{T,i}, f_L$ account for muon spin components perpendicular and parallel to the local field directions, experiencing relaxation rates $\sigma_i$ and $\lambda$, respectively, and obey $\sum_i f_{T,i} + f_L = 1$. Magnetic transitions are inhomogeneous and $v_m = 3(1 - f_L)/2 = 3(f_{T,1} + f_{T,2})/2$ measures the magnetic volume fraction (figure 8(d)).

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\[ B_1(h,T) = B_F \left[ 1 - \frac{h}{h_0} e^{-T_A/T} \right]^{\alpha} \left( 1 - T/T_N \right)^{\beta} \] (3)

where \( B_F = 30 \text{ mT} \) is the value of the local field at muon site 1 for \( T \to 0 \) and \( h = 0 \) (i.e., in the parent compound), exponents values are \( \alpha \approx 0.3, \beta \approx 0.15 \)–0.2, and fixed the critical hole number is \( h_c = 0.056(2) \), in agreement with the direct determination from \( T_N(h) \).

In this model \( T_x \) is a crossover temperature between a high temperature (\( T \to T_x \)) thermally activated regime, with plane mobile holes \( h \), and a low temperature frozen regime (\( T \ll T_x \)), clearly visible as an upturn [7, 17, 33] also in figure 8(e), where the holes localize.

Our model mimics the effect of the thermal excitations of the charge doped 2D Heisenberg quantum square antiferromagnet (2DHQSdAF) [34]. Hole activation is also reflected in a peak in the longitudinal relaxations \( \lambda \), clearly visible as an upturn [7, 17, 33] also in figure 8(e), where the holes localize.

Plane hole number may be thus determined from the known [17] dependence of \( T_N \) on \( h \) in YBa\(_2\)Cu\(_3\)O\(_{6+y}\):

\[ T_N(h) = T_{N0} \left[ 1 - \left( \frac{h}{h_0} \right)^2 \right] \] (4)

with \( T_{N0} = 422(5) \text{ K} \) and \( h_0 = 0.056(2) \). The best fit of the \( z = 0 \) sample data, figure 8(e), to equation (3) yields \( h = 0.026(2) \) and \( T_N = 320(15) \text{ K} \). The latter, inserted into equation (4) provides a value of \( h = 0.027(2) \), in perfect agreement with the best fit value. Remarkably, this method allows us to compute the plane hole number directly, since the magnetic properties are strictly influenced by local charge doping, in contrast to both transport measurements, sensitive to all mobile charges, and structural measurements, globally reflecting the changes in all layers.

Let us finally recall that the superconducting transition temperatures of the clean limit YBa\(_2\)Cu\(_3\)O\(_{6+y}\) are related [20] to 0.05 \( \leq h \leq h_{\text{opt}} = 0.16 \) by

\[ T_c(h) = 82.6/(h_{\text{opt}} - h)^2 \] (5)

4. Nuclear quadrupole resonance, chain length and plane hole count

In YBa\(_2\)Cu\(_3\)O\(_{6+y}\), the hole carrier number \( h \) depends on both \( y \) and sample preparation conditions. Reproducible values are obtained after very long annealing slightly above room temperature [35–37]. In annealed samples, like the ones investigated here, the average chain length \( \ell \) defined as the average number of oxygen ions in Cu(1)O chain fragments, depends only on oxygen content (\( y \)): filled Cu(1)O chains run along the orthorhombic crystal \( b \) direction for \( y \approx 1 \), and for decreasing oxygen content sequences of empty and filled chains tend to alternate regularly along \( a \) forming well defined superstructure. Below a critical threshold (\( y_c \approx 0.30 \) for YBa\(_2\)Cu\(_3\)O\(_{6+y}\)), \( y_c \) known to depend on the average cation radius, short fragments of chains become orientationally unordered [18, 19, 38–40]. This condition marks the T-O phase transition and identifies a critical chain length \( \ell_c \), also dependent on cation radius.

4.1. Chain length determination

The NQR resonance frequency of Cu, proportional to the electric field gradient at the nucleus, is characteristic of each inequivalent copper site in the lattice and very sensitive to nearest-neighbor (nn) oxygen configuration. Important nn configurations are Cu(1)-2 and Cu(1)-3, shown in the bottom inset of figure 9: the former is bonded only to two apical O ions, and it is surrounded by four O vacancies in the basal layer, the latter is bonded to an additional nn chain O, with three nn O vacancies. Since there are two Cu isotopes, \( ^{63}\text{Cu} \) and \( ^{65}\text{Cu} \), each configuration gives rise to a doublet, at the well known frequency \( (\nu_{63}/\nu_{65} = 1.082) \) and intensity \( (I_{63}/I_{65} = 2.235) \) ratios.

Two representative Cu(1) NQR spectra for the end members YBa\(_2\)Cu\(_3\)O\(_{6.35}\) (A) and EuBa\(_2\)Cu\(_3\)O\(_{6.35}\) (B) are shown in figure 9. The spectra are fitted to a sum of Voigt functions. According to a well established line assignment [12, 18, 27], the narrow doublet peak at 24 MHz and 22 MHz is due to the Cu(1)-3 configuration. The large peaks at \( \approx 22 \text{ MHz} \) is due to Cu(1)-4 sites from longer chain fragments.

Finer details are seen in the Y sample, where three distinct \( ^{65}\text{Cu} \) resonance peaks in the 29–32 MHz range and their very similar \( ^{63}\text{Cu} \) isotope replicas in the 27–29 MHz range correspond to as many different next-nearest-neighbor configurations of Cu(1)-2. They are shown in the top inset of figure 9: Cu(1)-2.0 surrounded by empty chains on both sides (at 30.1 and 27.8 MHz), Cu(1)-2.1, with one empty and one filled chain (at 30.6 and 28.3 MHz) and Cu(1)-2.2 with filled chains on both sides (31.1 and 28.7 MHz) [41]. The well resolved narrow resonances of the YBa\(_2\)Cu\(_3\)O\(_{6.35}\) sample testify that the three different local configurations are themselves quite homogeneous, as expected from the relatively high degree of order. On the contrary, these three peaks get broader and unresolved for the EuBa\(_2\)Cu\(_3\)O\(_{6.35}\) sample, indicating a greater degree of local disorder in the basal layer. This is further supported by the fact that for this sample the Cu(1)-3/Cu(1)-2 spectral weight ratio increases, indicating a relative abundance of the chain-end sites, i.e., the substitution of Eu yields to a shortening of the chain length at fixed oxygen content.

The chain length \( \ell \), shown in figure 10(c), is calculated from the weight of the two configurations (the area under each NQR peak doublet) as in [12, 18]
8

\[ \ell = 3/7(2A_2/A_3 + 1) \]  

4.2. Plane hole number calibration

In section 1.2 we assumed a linear relation, equation (1), between plane hole number \( h \) per \( \text{Cu}(2)\text{O}_2 \) square cell and the Eu content \( z \). We wish now to discuss the basis of this assumption.

Figures 10(a) and (b) shows the variation of the orthorhombic distortion coefficient \( (a-b)/(a+b) \) and the total hole count \( h_{\text{tot}} \), from the Seebeck data of table 1, versus the Y content \( z \). Both parameters are constant in the two distinct T and O structures and they both jump at the first order phase transition, for \( z = z_c \). By comparison the chain length \( \ell \) obtained by NQR with from equation (6) and shown in panel c varies linearly with \( z \) and is insensitive to the phase transition.

The hole transfer mechanism from the basal layer onto the \( \text{Cu}(2)\text{O}_2 \) planes requires the oxidation of \( \text{Cu}(1) \) from \( \text{Cu}^{1+} \) to \( \text{Cu}^{2+} \), but it becomes active only above a minimal chain length \( \ell_m \approx 2 \), \[18, 42\] after which both \( \ell \) and \( h \) increase. Heinma \textit{et al} \[41\] (see figure 5 therein) showed by NQR in \( Y_xR_{1-x}\text{Ba}_2\text{Cu}_3\text{O}_{y+3} \), that a linear dependence holds between  

\( \ell \) and oxygen content \( y \), with equal slope and slightly different intercepts in \( R_e = Y, \text{Gd} \). The two linear relation result in a direct proportionality between \( y \) and \( h \), which was experimentally established in \( \text{YBa}_2\text{Cu}_3\text{O}_{6+y} \), by the extensive single crystal work of Liang \textit{et al} \[20\], (notice that very accurate linearity holds in the underdoped regime relevant for the present work).

By the same argument we conclude that that the linear relation between \( \ell \) and \( z \), shown in figure 10(c), implies a linear scaling of \( h \) with \( z \), i.e. the validity of equation (1).

Recalling that the \( Y_x\text{Eu}_{1-x}\text{Ba}_2\text{Cu}_3\text{O}_{6.35} \) series displays a linear dependence on \( z \) for both the cell volume and the average lattice parameters, figure 2, it is reasonable to conclude that the steric hindrance of the Eu cation forces the \( \text{YBa}_2\text{Cu}_3\text{O}_{6.35} \)
lattice to a nearly isotropic dilation proportional to Eu content, which in turns determines the average chain length.

5. Discussion and conclusion: disorder influence on the phase diagram

The main result of this work is summarized in figure 11, where the transition temperatures in Y$_{x}$Eu$_{1-x}$Ba$_2$Cu$_3$O$_{6.35}$ are plotted versus hole concentration $h$, obtained according to the criteria of sections 1 and 3. Blue filled circles, open and filled triangles represent best fit Neél temperatures $T_N$, activation temperatures $T_A$ and freezing temperatures $T_f$, respectively, from the data of figure 8, by means of equation (3), while red filled circles are superconducting temperatures from SQUID measurements.

It is remarkable that, although the substitution parameter $z$ does not directly introduce a chemical doping, the phase diagram reproduces qualitatively the universal HTC cuprate behavior. A similar equivalence of chemical doping and structural distortion is well known in iron pnictides and selenides [43, 44], but is unprecedented in cuprates. The influence of disorder is shown by the deviations from the YBa$_2$Cu$_3$O$_{6+y}$ nearly clean-limit case, that is represented by the continuous orange and dashed white lines in figure 11(a) (referred to $h$, bottom axis). The difference is apparent when comparing the latter two curves with data (symbols) and their guide to the eye, delimiting the normalized suppression of $T_N$ (referred to by the continuous orange and dashed white lines in figure 11(a))

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We start by noticing that in cuprates values of $h$ of just few percent are sufficient to suppress $T_N$. This dramatic hole doping effect, much more effective than moment suppression by dilution [45], is due to frustration in the Néel state of the 2DHQSAF, introduced by the spin-hole excitations [34]. The rather strong additional reduction due to disorder (point (i)) is surprising, since both magnetic moments on Cu and their exchange couplings are virtually unaffected by the Y-Eu substitution. This suggests that quenched disorder influences directly spin-hole excitation, possibly by pinning, thus introducing additional frustration. The numerical work available to date [6] does not allow a direct comparison with our data. This calls for further theoretical work on the excitations of the 2DHQSAF in the presence of extra charge carriers and disorder.

Point (ii) confirms the progressive opening of a spin glass gap in the weak disorder regime, already observed for strong disorder in Y$_{1-x}$Ca$_x$Ba$_2$Cu$_3$O$_{6+y}$. The onset spin glass temperatures $T_f$ of the 0.6 $\leq z \leq$ 1.0 samples fall on a straight $T_A(h)$ line from the clean $z = 0$ value of $T_A$, exactly like in [7, 17]. The normalized suppression of $T_N$ and $T_A$, defined as

\[ \Delta T_N = 1 - T_{N,A}(h,z)/T_{N,A}(h,0) \]

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Let us finally consider point (iii), the shift of the onset concentration for superconductivity under increased quenched disorder. It is small, but outside errorbars and surprisingly negative: disorder seems to favour superconductivity. It is tempting to argue that the suppression of the 2DHQSAF provides an increased spin density of state involved in the superconducting pairing, but in Y$_{1-x}$Ca$_x$Ba$_2$Cu$_3$O$_{6+y}$ the same shift was comparable and positive, seemingly in contradiction with this argument. A tentative explanation is to consider that the onset of superconductivity actually coincides, within the accuracy of the present study, with the T-O transition as it does in pure YBa$_2$Cu$_3$O$_{6+y}$. The locking of the $T_c$ onset and the structural transition emphasizes the role of nematic susceptibility [46] in unconventional superconductivity.
Acknowledgments

We thank Edi Gilioli and Francesca Licci for useful discussions on sample preparation and characterization, Alex Amato and James Lord for support in the μSR experiments, We gratefully acknowledge the Science and Technology Facilities Council (STFC) and the Paul Scherrer Institut, Villigen, Switzerland for access to their muon beamtime at ISIS and LMU. Work supported in part by UniCa, Fondazione di Sardegna, and Regione Autonoma della Sardegna via Progetto biennale di ateneo 2016 Multiphysics approach to thermoelectricity, by CINECA, Bologna, Italy through ISCRA Computing Grants, and by CRS4 Computing Center, Piscina Manna, Italy.

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