3D Global Coronal Density Structure and Associated Magnetic Field near Solar Maximum

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ABSTRACT

Measurement of the coronal magnetic field is a crucial ingredient in understanding the nature of solar coronal dynamic phenomena at all scales. We employ STEREO/COR1 data obtained near maximum of solar activity in December 2012 (Carrington rotation, CR 2131) to retrieve and analyze the three-dimensional (3D) coronal electron density in the range of heights from 1.5 to 4 R\(_{\odot}\) using a tomography method and qualitatively deduce structures of the coronal magnetic field. The 3D electron density analysis is complemented by the 3D STEREO/EUVI emissivity in 195 Å band obtained by tomography for the same CR period. We find that the magnetic field configuration during CR 2131 has a tendency to become radially open at heliocentric distances below \(\sim 2.5\) R\(_{\odot}\). We compared the reconstructed 3D coronal structures over the CR near the solar maximum to the one at deep solar minimum. Results of our 3D density reconstruction will help to constrain solar coronal field models and test the accuracy of the magnetic field approximations for coronal modeling.

Subject headings: Sun, corona, electron density, magnetic field, tomography

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1. Introduction

Solar coronal magnetic field is a major source of dynamics and thermodynamics of global coronal corona and transient coronal events including the coronal heating, solar flares, coronal mass ejections and the solar wind. Its dynamics affects space weather processes that may impact Earth’s magnetosphere and atmosphere and affect life on our planet. Thus, the knowledge of coronal magnetic field strength and topology represents one of major goals of the solar physics. Currently, coronal magnetic fields cannot directly measured. The major techniques that are currently used to derive the global magnetic structures of the solar corona represent indirect methods including potential field source surface (PFSS) models, non-linear force-free field (NLFFF) models and multi-dimensional magnetohydrodynamic (MHD) models of the global solar corona. These methods use solar photospheric scalar or vector magnetic field as input directly derived from photospheric magnetograms. However, as we discussed in Kramar et al. (2014), all these methods cannot adequately describe the dynamics of magnetic fields observed in the solar corona driven by current carrying structures. Moreover, they do not provide accurate information about the coronal thermodynamics, and thus cannot be used for modeling the coronal emission measures derived from extreme ultraviolet (EUV) observations. The MHD modeling of the solar corona provides a self-consistent time-dependent treatment of the plasma pressure, gravitational and magnetic forces, but are limited by approximations used for describing the coronal heating, and the uncertainties in the boundary conditions that are deduced from synoptic data. Thus, direct measurements of the coronal magnetic field remains one of the most reliable and challenging ways for characterization of solar coronal processes.

Direct measurement of the coronal magnetic field is the most challenging problem in observational solar physics. A major progress here was reached with the deployment of the Coronal Multichannel Polarimeter (CoMP) (Tomczyk et al. 2007, 2008). In order to interpret such type of data, a vector tomography method has been developed for 3D reconstruction of the global coronal magnetic field (Kramar et al. 2006, 2013), and recently, first 3D reconstruction of the global coronal magnetic field has been performed based on the CoMP data (Kramar et al. 2016).

Another, thought implicit but also based on coronal observations, way to reconstruct some global coronal magnetic field structures was investigated in Kramar et al. (2014). There we applied the tomography method that employs STEREO data to reconstruct 3D density of global solar corona and related it to the coronal magnetic field structure. This method was applied to characterize the solar corona over the Carrington rotation 2066 occurred during deep solar minimum for the range of coronal heights from 1.5 to 4 R_<☉> and provided description of the open/close magnetic field boundaries in the solar corona.
In this paper, we apply this methodology to study global solar coronal structures for the period of over the half of Carrington rotation 2131, which represents the case of solar maximum. Specifically, we use the STEREO/COR1 coronagraph data for half a solar rotation period during CR 2131 as input for the tomographic reconstruction of the 3D coronal electron density and the configuration of magnetic field associated with them. Our results are complemented by the 3D emissivity obtained by tomography method applied for the the STEREO Extreme Ultraviolet Imager (EUVI) data in the 195 Å band. We also compared the reconstructed 3D coronal structures with those implied by the PFSS model. In Section 4, we present the comparison of the 3D coronal structure near the solar maximum to those at deep solar minimum (CR 2066).

2. Methods

The corona is optically thin at visible and EUV wavelengths dominated by lines of ionized iron and calcium. Thus, the observed visible and EUV coronal flux represents an integral of the emissivity along any line of sight (LOS). This makes it impossible to reconstruct the spatial distribution of the emissivity from a single (in a geometric sense) measurement or projection. The solution space is reduced if we have measurements from many different viewpoints. The three-dimensional (3D) reconstruction of optically thin emission over depths can be performed by using tomography methods that employ the 2D observations of an object from different view angles. The possibility of reconstructing a function from its projections was first studied by [Radon (1917)]. Several decades later, this purely mathematical method formed the basis for the X-ray computer tomography that produces cross-sectional slices of human bodies ([Cormack 1963, 1964] and [Hounsfield 1972]). Today, tomography is used in many fields of science including medical research, material structure testing, geophysics, heliophysics and astrophysics ([Boffin et al. 2001]). In astrophysical applications the input data can suffer from noise and data incompleteness. While the application of tomography to astrophysical objects is limited by the noisy input data and its incompleteness, the regularization method allows solar coronal tomography to produce reliable 3D reconstructions of emissivity and plasma density ([Tikhonov 1963; Frazin & Janzen 2002; Kramar et al. 2006, 2009]).

2.1. Tomography Based on White-Light STEREO/COR1 Data

The key input for tomographic reconstruction of the plasma density of extended solar coronal structures requires observational data from more than two vantage points. To-
mography applications for coronal studies typically assume a rigid rotation of the coronal density structures. For reliable density reconstruction, the algorithm utilizes coronagraph data for half a solar rotation as input if observed from a single spacecraft and requires coronal structures to remain stable over their observation periods (Davila 1994; Zidowitz 1999; Frazin & Kamalabadi 2005; Kramar et al. 2009). However, depending on the positions of a coronal structure relative to the spacecraft during the observation period, the stationarity assumption for that structure can be reduced to about a week (Kramar et al. 2011).

For our density reconstructions we used the polarized brightness (pB) intensity images from the COR1 instrument onboard the STEREO-B spacecraft taken 28 images per half a solar rotation as input for the tomographic inversion. We limited here the data input for the tomography based on COR1 data to the STEREO-B spacecraft because COR1-B had lower levels of stray light during CR 2066 than COR1-A.

In the STEREO/COR1-B field of view (below $\approx 4 R_\odot$), the white-light pB coronal emission is dominated by scattering sunlight on the free electron in the corona (Blackwell & Petford 1966a, b; Moran et al. 2006; Frazin et al. 2007). The intensity of the pB-signal as a fraction of the mean solar brightness is given as

$$I_{pB}(\hat{e}_{\text{LOS}}, \rho) = \int_{\text{LOS}} K(r) N_e(r) d\ell,$$

where $N_e$ is the electron density, $\rho$ is a vector in plane-of-sky (POS) from the Sun center to the LOS and perpendicular to LOS, $\ell$ is length along the LOS, $\hat{e}_{\text{LOS}}$ is the unit vector along the LOS, and $r$ is the radius-vector. The kernel function $[K]$ is defined by the Thompson scattering effect (van de Hulst 1950; Billings 1966; Quémerais & Lamy 2002):

$$K = \frac{\pi \sigma}{2} \left( \frac{1}{1 - \frac{u}{3}} \right) \left[ (1 - u) A(r) + u B(r) \right] \frac{\rho^2}{r^2},$$

where the expressions for $A(r)$ and $B(r)$ are the same as those given by Quémerais & Lamy (2002), $\sigma = 7.95 \times 10^{-26}$ cm$^2$ is the Thompson scattering cross-section for a single electron, and the linear limb-darkening coefficient $[u]$ is set to 0.6 in the present calculations.

Because COR1 views the corona close to the limb, the instrument has a significant amount of scattered light, which must be subtracted from the image prior to be applied in the reconstruction method. Proper removal of instrumental scattered light is essential for coronal reconstruction. One way is to subtract a monthly minimum (MM) background. The monthly minimum approximates the instrumental scatter by calculating the lowest value of each pixel in all images during a period of about one month. However, this method tends to overestimate the scattered light in the streamer belt (equatorial region). The lowest value
of these pixels during a month usually contains both the scattered light and the steady-intensity value from the corona. Hence, the subtraction of MM background would output an electron density in streamer regions that is lower than the actual density.

Another way to account for the scattered light is to subtract a roll minimum (RM) background. The roll minimum background is the lowest value of each pixel obtained during a roll maneuver of the spacecraft (instrument) around its optical axis. Because the coronal polar regions are much darker than the equatorial ones, the lowest pixel values in the equatorial region during the roll maneuver are nearer to the value of the scattered-light intensity than the MM.

The sensitivity of the COR1-B instrument decreases at a rate of about 0.25 % per month (Thompson & Reginald 2008). Moreover, variations in the spacecraft’s distance from the Sun cause changes of the amount of scattered light in the coronagraph images. But the roll manoeuvres are done rarely. Therefore, it is impossible to use an RM background obtained in one month for data for the following month when the highest possible photometric accuracy is needed. A background image for the period between the roll manouevres can be derived from interpolation of the RM backgrounds over time in such a way that this temporal dependence follows the temporal dependence of the MM backgrounds, because the MM background images are available for every month. In our study we used the approach implemented by W. Thompson in the SolarSoft IDL routine secchi_prep with the keyword parameter calroll.

The photometric calibration is based on Jupiter’s passage through the COR1 FOV (Thompson & Reginald 2008).

After subtracting the scattered light, a median filter with a width of three pixels was applied to reduce anomalously bright pixels caused by cosmic rays. Then, for the CR 2066 reconstruction, every third image pixel was selected (resulting in a 340 × 340 pixel image from original 1024 × 1024) to reduce the computer memory size. In case of CR 2112 and 2131 reconstructions, we used original 512 × 512 input data resolution. We used the reconstruction domain as a spherical grid with a size of 50 × 180 × 360 covering heliocentric distances from 1.5 to 4 R⊙, Carrington latitudes from −90 to 90°, and Carrington longitudes from 0 to 360°, respectively.

The inversion was performed for the function

\[
F = |A \cdot X - Y|^2 + \mu |R \cdot X|^2.
\]  

(3)

Here, the elements \(x_j\) of the column matrix \(X\) contain the values of electron density \([N_e]\) in the grid cells with index \(j = 1, ..., n\), and \(y_i\) is the data value for the \(i\)-th ray, where index \(i = 1, ..., m\) accounts for both the viewing direction and pixel position in the image.
element $a_{ij}$ of the matrix $A$ represents the intersection of volume element $j$ with LOS related to pixel $i$, multiplied by the kernel function that is defined by the Thompson scattering effect for the pB-intensity signal (see Equation (1)). The second term on the right-hand side of Equation (3) is the regularization term that minimizes the effects of noise and data gaps (Tikhonov 1963). The matrix $R$ is a diagonal-like matrix such that the regularization is the first-order smoothing term, i.e. operation $|R \cdot X|^2$ produces the square difference in value between two neighboring grid cells, summed over all cells. The regularization parameter $[\mu]$ regulates balance between the smoothness of the solution on one hand and the noise and reconstruction artifacts on the other. The result of the inversion depends on a number of factors, including the number of iterations and the value of $\mu$. The value of $\mu$ was chosen using the cross-validation method (Frazin & Janzen 2002). The iterations are performed until the first term in Equation (3) became slightly lower than the data noise level, which is essentially the Poisson noise in the data.

The coronal electron density drops very rapidly with distance from the Sun, introducing a wide dynamic range in the data, which causes linear artifacts in the reconstruction. To increase the contribution of signals from those LOS that pass through the low density regions, and to reduce the artifacts in the numerical reconstruction at larger distances from the Sun, we applied a set of weighting coefficients (or preconditioning)

$$w_i = \frac{1}{\left( y_i^{(FT1)} \right)^2}$$

(4)

were applied for the first term in Equation (3) in such way that $\sum_j (w_i a_{i,j} x_j) = w_i y_i$. Here, $y_i^{(FT1)}$ is the inverse Fourier transform of the function $y_i(r_p, \phi_p)$ on $\phi_p$ with harmonics taken up to first order, where $y_i(r_p, \phi_p)$ is the data value at the position $(r_p, \phi_p)$ in the polar coordinate system for some particular image. The value of $r_p$ is fixed for a given pixel and set equal to the radial distance from the center of the Sun’s disk to the pixel. A more detailed description of used tomography method is given in Kramar et al. (2009). The reconstruction results are discussed in Section 3.

### 2.2. Tomography for Emissivity from STEREO/EUVI Data

The STEREO/EUVI instrument observes the solar corona at heights up to about 1.7 $R_\odot$ in four spectral channels (171, 195, 284, and 304 Å) that span the 0.1 to 20 MK temperature range (Wuelser et al. 2004, Howard et al. 2008). The measured coronal emission in the 171,
195, and 284 Å channels can be represented as the result of emission integrated over the LOS as

\[ I(\tilde{e}_{\text{LOS}}, \rho) = k \int_{\text{LOS}} \varepsilon(r) \, d\ell, \]  

where \( \varepsilon(r) \) is the emissivity at the position \( r \) in the selected channel, \textit{i.e.} light intensity (in photons per second for example) emitted per unit volume, per unit solid angle. The coefficient \( k \) accounts for pixel size, aperture, and distance to the Sun.

As input, we used EUVI 195 Å images calibrated by applying IDL SolarSoft routines. To reduce anomalously bright pixels caused by cosmic rays, the IDL SolarSoft routine \texttt{de-spike_gen} was applied. Three images taken with about two hours difference were averaged into one. Three averaged images per day were taken during a period of half a solar rotation. Then, every fourth pixel was taken, resulting in \( 512 \times 512 \) input image.

We inverted \( \varepsilon(r) \) in the same manner as for the electron density in the white-light tomography with \( K \) and \( N_e \) in Equation (1) substituted by \( k \) and \( \varepsilon \), respectively, according to Equation (5). The inversion result is the 3D emissivity distribution for the EUVI 195 Å channel in the coronal range from 1.05 to 1.5 \( R_\odot \). Figure 2 shows a spherical cross-section of the reconstructed EUVI 195 Å emissivity at a heliocentric distance of 1.1 \( R_\odot \) for CR 2131. The reconstruction results are discussed in Section 3.

### 3. 3D Coronal Structure during CR 2131

CR 2131 represents the period near maximum of solar activity cycle. In this study, we performed two types of tomographic reconstructions: 3D reconstruction of the electron density based on STEREO/COR1 data and 3D reconstruction for the EUVI 195 Å emissivity [units of photons s\(^{-1}\) sr\(^{-1}\) cm\(^{-3}\)] based on STEREO/EUVI data. In order to demonstrate a general structure of the coronal streamer belt for CR 2131, Figure 1 shows a spherical cross-section of the electron density at the heliocentric distance of 2 \( R_\odot \), and Figure 2 shows a spherical cross-section of the EUVI 195 Å emissivity at the heliocentric distance of 1.1 \( R_\odot \).

Figure 3 shows several meridional cross-sections of the electron density (range from 1.5 to 4 \( R_\odot \)) and EUVI 195 emissivity (range from 1.05 to 1.29 \( R_\odot \)). The figure with a set of all cross-sections is available in the Electronic Supplemental Material.

The black contour lines in Figure 3 show boundaries between open and closed magnetic-field structures in two PFSS models with Source Surface heliocentric distances \( [\text{R}_{\text{SS}}] \) at 1.5 and 2.0 \( R_\odot \). The PFSS model with \( \text{R}_{\text{SS}} = 2.0 \ R_\odot \) does not coincide with the derived positions of the streamer and pseudo-streamer as well as with the coronal hole positions.
indicated by the STEREO/EUVI 195 Å emissivity 3D reconstruction. The PFSS model with \( R_{ss} = 1.5 R_\odot \) appears to fit the latter structures better.

It was previously demonstrated that the position of maximal gradient of the density and 195 Å emissivity can be an indicator for the position of boundary between closed and open magnetic structures Kramar et al. (2014). Therefore, in order to exhibit the possible real boundary positions, Figure 4 shows gradient of electron density and EUVI 195 emissivity, \( \partial N_e / \partial \theta \) and \( \partial \epsilon_{195} / \partial \theta \), for CR 2131 and for the same longitudinal cross-sections as in Figure 3. Both Figures 3 and 4 demonstrate that the magnetic field configuration during CR 2131 has a tendency to become radially open at heliocentric distances below \( \sim 2.5 R_\odot \). This is lower than corresponding distance during the deep solar minimum near CR 2066 (Kramar et al. 2014).

Figure 5 shows the radial profiles of the maximum (left panel) and average (right panel) electron density values at different heliocentric distances for CR 2066 (dashed green), 2112 (solid red), and 2131 (solid black). CR 2066 corresponds to deep solar minimum, while CR 2131 corresponds to period near solar maximum. The maximum values of coronal density mostly reflect the closed magnetic field structures represented by solar active regions, while average values include contributions from both open and closed field regions. The plot suggests that the maximum coronal density at the solar maximum is larger than the coronal density at two Carrington rotations representing the periods of lower magnetic activity. Specifically, at the lower boundary (at 1.8 \( R_\odot \)) of the reconstruction region the maximum density at solar maximum is more than twice greater than the maximum coronal density at solar minimum represented by CR 2066. This reflects the fact that the total unsigned magnetic flux that is structured in the form of coronal active regions during solar maximum is a factor of 2-3 greater than the emerging magnetic flux during solar minimum (Solanki et al. 2002). The average coronal density is a factor of 1.6 greater during solar maximum as compared to solar minimum, because it reflects the contribution of plasma emission formed in the diffuse corona as well as coronal active regions.

Figure 6 shows the snapshot of the isosurface of coronal electron density value of \( 10^6 \text{cm}^{-3} \) (in blue) for CR 2066 occurred at solar minimum (left) and CR 2131 at solar maximum (right). The corresponding movie showing the density isosurface over these two Carrington rotations are available provided in online version of the paper. The figure and the movie clearly demonstrate that the filling factor of the plasma with the density of \( 10^6 \text{cm}^{-3} \) increases at solar maximum, which is consistent with Figure 5.
4. Conclusion and Outlook

We applied the tomography method to STEREO-B/COR1 data to derive the reconstructions of the 3D global coronal electron density and EUVI 195 Å emissivity based on STEREO/ COR1 and STEREO/EUVI observations near solar maximum represented by Carrington rotation CR 2131 (December 2012). We complemented the tomography with MHD simulations to obtain the open/closed magnetic field boundaries in the solar corona. Because the 3D reconstructions are based entirely on coronal data, these results could serve as an independent test and/or as an additional constraint for the models of the solar corona. Specifically, we used the PFSS model for different source surface distances as a test case for the reconstructed 3D electron density and EUVI 195 emissivity structures.

We have shown that magnetic field structures deviate significantly from the PFSS approximation as evident from the derived boundaries of open/closed field for both solar minimum (Kramar et al. 2014) and solar maximum. This suggests that potential field approximation for the low corona is not a valid approximation when describing its large-scale structures. It is important to note that the magnetic field becomes radial at heights greater than $2.5R_\odot$ during solar minimum, while its open up at heights below $\sim 2.5R_\odot$ during solar maximum.

Our studies also show that the average and the maximum electron densities in the low solar corona at heights $\sim 1.8R_\odot$ are about 2 times greater than that obtained during solar minimum. This is an important result that can be extrapolated to coronal densities of active and young solar-like stars. These stars show much greater levels of stellar activity in terms of at $> 10$ times greater surface magnetic flux, up to 1000 times more luminous in X-rays and at least 10 times denser and hotter corona. These results open up an interesting opportunity to provide scaling of the electron density of the solar corona with different levels of magnetic activity traced by its X-ray luminosity and average surface magnetic flux. These scaling laws can be then used for characterization of stellar corona of active stars, which may provide insights on the nature of stellar coronal heating at various phases of their evolution.

Applied in this study method can also be used for verification of 3D global coronal vector magnetic field obtained by vector tomography based on coronal polarimetric observations (Kramar et al. 2016).

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Fig. 1.— Spherical cross-section of the reconstructed electron density in square root scale at heliocentric distance of $2 \, R_\odot$. The reconstruction is obtained by tomography based on COR-1 data obtained during December 4-17, 2012 (CR 2131). Solid black and dashed red lines indicate the magnetic neutral line in PFSS model with source surface located at 1.5 and $2 \, R_\odot$, respectively.
Fig. 2.— Spherical cross-section of the reconstructed 3D EUVI 195 Å emissivity in square root scale at heliocentric distances of 1.1 $R_\odot$. The reconstruction is obtained by tomography based on COR-1 data obtained during December 4-17, 2012 (CR 2131). Solid black and dashed red lines indicate the magnetic neutral line in PFSS model with source surface located at 1.5 and 2 $R_\odot$, respectively.
Fig. 3.— Reconstructions for CR 2131 based on COR1 data (electron density in the range from 1.5 to 4 $R_\odot$) and EUVI 195 Å data (emissivity in the range from 1.05 to 1.29 $R_\odot$). Carrington longitudes for cross-sections are shown at upper right corners. The figure with a set of all cross-sections is available in the Electronic Supplementary Material. The contour black lines show boundaries between open and closed magnetic-field structures for the PFSS models with Source Surface located at 1.5 and 2.0 $R_\odot$. 
Fig. 4.— Longitudinal cross-sections of gradient of electron density and EUVI 195 emissivity, \(\partial N_e/\partial \theta\) and \(\partial \varepsilon_{195}/\partial \theta\), for CR 2131. Carrington longitudes for cross-sections are shown at upper right corners. Color scales are different for different cross-sections to enhance the images. The contour black lines show boundaries between open and closed magnetic-field structures for the PFSS models with Source Surface located at 1.5 and 2.0 \(R_\odot\).
Fig. 5.— Maximal (left panel) and average over a spherical surface area (right panel) electron density values at different heliocentric distances for CR 2066 (dashed green), 2112 (solid red), and 2131 (solid black). CR 2066 corresponds to deep solar minimum, while CR 2131 corresponds to period near solar maximum.

Fig. 6.— Isosurface of coronal electron density value of $10^6$ cm$^{-3}$ (in blue) for CR 2066 (left) and 2131 (right). The orange sphere is located at 1.5$R_\odot$ just for scaling purpose. The movie demonstrating the isosurfaces for the whole longitudinal projection range is provided in online version of the paper.