Mapping anomalous dispersion of air with ultrashort mid-infrared pulses

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We present experimental studies of long-distance transmission of ultrashort mid-infrared laser pulses through atmospheric air, probing air dispersion in the 3.6–4.2-μm wavelength range. Atmospheric air is still highly transparent to electromagnetic radiation in this spectral region, making it interesting for long-distance signal transmission. However, unlike most of the high-transmission regions in gas media, the group-velocity dispersion, as we show in this work, is anomalous at these wavelengths due to the nearby asymmetric-stretch rovibrational band of atmospheric carbon dioxide. The spectrograms of ultrashort mid-infrared laser pulses transmitted over a distance of 60 m in our experiments provide a map of air dispersion in this wavelength range, revealing clear signatures of anomalous dispersion, with anomalous group delays as long as 1.8 ps detected across the bandwidth covered by 80-fs laser pulses.

Atmospheric optics is one of the earliest fields not only in optics, but among all the natural sciences1–2. As a branch of knowledge dealing with an observation and explanation of the colors of the sky, rainbows, halos, and mirages, it was exclusively concerned with the visible light and the visible spectral range, where atmospheric air is highly transparent. Systematic studies of radiation propagation in Earth’s atmosphere, motivated by the needs of observational astrophysics and performed with an ever-increasing experimental accuracy over many centuries3, helped achieve a detailed quantitative understanding of atmospheric transmission in the visible region.

In the era of ultrafast laser technologies, enabling the generation of high-power ultrashort field waveforms within an ultrabroad spectral range from the visible to the mid-infrared, a deeper understanding of the group-velocity dispersion (GVD) of atmospheric air is needed. This call includes a quest for anomalous-GVD ranges as a top priority for long-distance signal transmission and remote sensing of the atmosphere. Anomously dispersive materials play a very special role in ultrafast optical science. Acting jointly with optical nonlinearity, anomalous dispersion gives rise to a vast variety of soliton phenomena4. In its one-dimensional version, this type of nonlinear dynamics has long been known in fiber optics5, enabling long-distance signal transmission and fiber-optic communications6, as well as short-pulse generation in fiber lasers7. Pulse compression in anomalously dispersive fibers6 has recently been extended to fiber-format subcycle pulse generation8. In anomalously dispersive bulk solids, spatial localization provided by spatial self-action and laser filamentation can be combined with temporal field confinement due to a solitonic dynamics of laser pulses8. With a careful optimization, this spatiotemporal field localization in anomalously dispersive solids enhances compression of high-peak-power mid-infrared laser pulses9 and can help generate light bullets as a part of laser-induced filamentation10. If extended to atmospheric air, these regimes would open unique opportunities for a long-distance transmission of high-peak-power laser pulses and remote sensing of the atmosphere. However, because of a complicated behavior of atmospheric refractivity within and near molecular absorption lines, identifying the ranges where atmospheric air would be both anomalously dispersive and still transparent is anything but trivial12.

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Here, we present experiments on long-distance transmission of ultrashort mid-infrared laser pulses through atmospheric air, probing air dispersion in the 3.6–4.2-μm wavelength range. Atmospheric air is still highly transparent to electromagnetic radiation in this spectral region, making it interesting for long-distance signal transmission.  However, unlike most regions of high transmission in gas media, dispersion anomalies are possible at these wavelengths due to the nearby asymmetric-stretch rovibrational band of atmospheric CO₂. Our experiments reveal clear signatures of anomalous GVD in this wavelength range, with group delays as long as 1.8 ps detected across the bandwidth covered by 80-fs laser pulses.

To analyze the dispersion of atmospheric air in the 3.6–4.2-μm wavelength range, we calculate the refractive index of air as

\[ n(\omega) \approx 1 + \frac{e^2}{2m_e \varepsilon_0} \sum_{k,i} N_k \frac{f_k (\omega_i)}{2\omega_i} \left( [D_k(\omega)]^{-1} - [D_\omega(\omega)]^{-1} \right) + n_{\text{in}}(\omega) \]

where \( \omega \) is the frequency, \( N_k \) is the density of molecules of sort \( k \), \( \omega_{ki} \) \( f_k(\omega) \) \( f_{ki}(\omega_i) \) \( D_k(\omega) \) \( D_\omega(\omega) \) \( n_{\text{in}}(\omega) \) are the frequency, the linewidth, and the oscillator strength of the ith resonance in the spectrum of molecules of sort \( k \), \( m_e \) and \( e \) are the electron mass and charge, \( \varepsilon_0 \) is the dielectric permittivity of vacuum, \( D_k(\omega) = \omega + \omega_{ki} - i\Gamma_k/2 \), \( D_\omega(\omega) = \omega - \omega_{ki} - i\Gamma_k/2 \), and \( n_{\text{in}}(\omega) \) is the refractive index of air in the visible–near-infrared range, calculated with the standard formula \(^{14,15} \)

\[ n(\lambda) = n(\omega) \approx 1 - \frac{\omega^2}{\omega_p^2} - \frac{\omega^4}{\omega_p^4} \]

In the full model of air refractivity, we calculate the refractive index of air with Eq. (1) including the entire HITRAN-database manifold of molecular transitions in air\(^{16} \). The GVD of atmospheric air can then be found as \( \kappa_\omega = \partial^2 \delta(\omega)/\partial \omega^2 \), where \( \kappa_\omega = 2n(\omega)/c \) is the speed of light in vacuum, and \( n(\omega) \) is calculated using Eq. (1). Dispersion of atmospheric air within the 3.5–4.2-μm wavelength range is dominated by the 00°01–00°11 asymmetric-stretch rovibrational band of atmospheric CO₂ (here, the \( \nu R,\nu P \) notation is adopted for a superposition of \( \nu_R \) symmetric-stretch, \( \nu_P \) bending, and \( \nu_v \) asymmetric-stretch vibrations with an angular momentum \( l \), and Fermi-resonance perturbation parameter \( r \)). The frequencies of rovibrational transitions within the P and R branches of this molecular band are given, within the standard approximation\(^{15,16} \), by \( \omega_{R,P}(J) \approx \omega_0(J \pm 1) - \omega_{\nu}(J) \) with \( \omega_0(J) \approx G_{\text{00}} + B_{\text{00}}(J + 1) \), where \( G \) are the vibrational terms and \( B \) are the rotational constants of a molecule, \( J \) and \( \nu \) being the rotational and vibrational quantum numbers, respectively. For the 00°01–00°11 mode of CO₂, \( G_{\text{00}} = 0, G_{\text{00}} \approx 442.80300 \) \( \text{rad/ps} \), and \( B_{\text{00}} \approx 0.072974425 \) \( \text{rad/ps} \).

The intensities of individual spectral peaks within the P and R branches of the 00°01–00°11 CO₂ band, related to the oscillator strength by \( f_{ki} = f_{R,P}(J, T) = (4\pi^2 \varepsilon_0 c^2)^{-1} S_{R,P}(J, T) \), are given by\(^{19} \)

\[ S_{R,P}(J, T) = \frac{\omega_{R,P}(J) f_{R,P}(J)}{\omega_0} \exp(-\hbar \omega_0(J)/kT) \exp(-\hbar \Delta \omega_{\text{R},\text{P}}(J)/kT) \]

where \( T \) is the temperature, \( \omega_0 = G_{\text{00}} - G_{\text{00}} \) \( S_0(T) \) is the line strength, \( L_{R,P}(J) \) is the Hönig–London factor, \( Q(T) = \Sigma(2J + 1) \exp(-\hbar \Delta \omega_{\text{R},\text{P}}(J)/kT) \) is the rotational partition sum, \( \kappa \) is the Boltzmann constant, and \( h \) is the Planck constant.

In Fig. 1a and b, we plot the refractive index and the GVD of atmospheric air within the 4.2–4.3-μm wavelength range of CO₂. \( G_{\text{00}} \approx 442.80300 \) \( \text{rad/ps} \), \( B_{\text{00}} \approx 0.073554528 \) \( \text{rad/ps} \), \( G_{\text{00}} \approx 442.80300 \text{rad/ps} \), and \( B_{\text{00}} \approx 0.072974425 \text{rad/ps} \).

It is, however, the high-frequency wing of this molecular band, stretching from approximately 3.5 to 4.2 μm, that we identify here as the region that offers unique options for the ultrafast optics of the atmosphere. Here, unlike the central part of the CO₂ absorption band, where the attenuation length is as short as \( l_\text{a} \approx 1 \) m at \( \lambda = 4.26 \) μm, atmospheric air is already highly transparent, with the attenuation length at our laser wavelength of 3.9 μm estimated as \( l_\text{a} \approx 40 \) km. Remarkably, in contrast to most of the high-transmission regions in gas media, the GVD is anomalous in this region (Fig. 1b,c). This unique combination of high transmission and anomalous GVD is achieved due to the high probabilities of rovibrational transitions within this molecular band, expressed by the high integral oscillator strength of the entire band.

Due to the large \( f_{ki}(J, T) \) within the P and R branches of the 00°01–00°11 band of CO₂, the anomalous GVD provided by the second term in Eq. (1) for \( \omega > \omega_{\nu}(J) \) prevails over the normal GVD due to the \( n_{\text{in}}(\omega) \) term, which dominates the GVD within the entire visible and most of the near-infrared range. As can be seen from Fig. 1b and c, right outside the CO₂ absorption band, i.e., for \( \lambda < 4.2 \) μm, the net GVD remains anomalous within the bandwidth that is broad enough to support pulses as short as ~200–250 fs.

The net GVD calculated by using Eq. (1) that includes only the 00°01–00°11 band of atmospheric CO₂ with density \( N_{\text{CO}_2} \approx 1.32 \times 10^{18} \text{cm}^{-3} \) is shown by the blue line in Fig. 1c. It seems to provide a significantly anomalous GVD everywhere within the 3.5–4.2-μm range. However, when other major molecular atmospheric constituents, primarily \( \text{H}_2\text{O}, \text{O}_3 \), and \( \text{CH}_4 \), are added to the sum in \( k \) in Eq. (1), with their densities \( N_k \) taken at normal conditions \( (N_{\text{H}_2\text{O}} \approx 5.4 \times 10^{14} \text{cm}^{-3}, N_{\text{O}_3} \approx 2.5 \times 10^{15} \text{cm}^{-3}, \text{and } N_{\text{CH}_4} \approx 4.0 \times 10^{14} \text{cm}^{-3} \), the GVD behavior within the 3.5–4.2-μm range becomes much more complicated. Now, the high-frequency negative-GVD tail provided by the 00°01–00°11 CO₂ band is observed against oscillatory GVD features related primarily to \( \text{H}_2\text{O}, \text{O}_3 \), and \( \text{CH}_4 \) molecules (red line in the upper panel of Fig. 1c). These features are almost invisible in \( \Delta n(\omega) \) and \( \kappa_\omega \) in Fig. 1a and b, but show up in the blowup of the GVD profile in Fig. 1c.

To understand the significance of these small-scale oscillatory GVD features for the dynamics of ultrashort mid-infrared pulses, we examine the temporal evolution.
of a Gaussian laser pulse \( A_0(\eta) \) whose initial pulse width, \( \tau_0 = 80 \text{ fs} \), and central wavelength, \( \lambda_0 = 3.9 \mu\text{m} \), are chosen in such a way as to model laser probe pulses in our experiments. The kernel in the time-evolution integral,

\[
G(\eta) = \int_0^\infty \exp(i\omega t - ik(\omega)z) d\omega,
\]

includes all the absorption and dispersion features of atmospheric air as shown in Fig. 1c.

Results of these calculations clearly show (Fig. 1e) that the small-scale oscillatory GVD features in the 3.5–4.2-\( \mu\text{m} \) range have no effect on the dynamics of ultrashort probe pulses in our experimental conditions, as they show up on a very long, ~10-ps time scale as extremely weak features, whose intensity is about eight orders of magnitude lower than the intensity of the laser probe (Fig. 1e). As is also seen in Fig. 1e, the temporal envelope of the transmitted laser pulse on the ~10–100-ps time scale is dominated by rotational echo revivals (e.g., those
centered at \( \eta \approx 55 \) and 100 ps in Fig. 1e) – a standard behavior of a laser probe in time-resolved studies of molecular rovibrational modes.\textsuperscript{20,21}

Ultrashort mid-IR pulses are delivered in our experiments by a laser system (Fig. 2) consisting\textsuperscript{22,23} of a solid-state ytterbium laser with an amplifier, a three-stage optical parametric amplifier (OPA), a grating–prism (grism) stretcher, a Nd: YAG pump laser, a three-stage OPCA system, and a grating compressor for mid-IR pulses. The 1-kHz, 200-fs, 1–2-mJ, 1030-nm regeneratively amplified output of the Yb: CaF\(_2\) laser system is used as a pump for the three-stage OPCA, which generates 1460-nm pulses at its output. These 1460-nm pulses are then stretched with a grism stretcher and used as a seed in a three-stage OPCA, consisting of three KTA crystals (Fig. 2), pumped by 100-ps Nd: YAG-laser pulses with energies 50, 250, and 700 mJ, respectively. The stretched-pulse idler-wave output of the OPCA system has a central wavelength of 3.9 \( \mu \)m and an energy up to 50 mJ. Compression of these pulses using a grating compressor yields mid-IR pulses with a pulse width of 80 fs and an energy up to 30 mJ.

To provide a long propagation path of a mid-infrared beam through atmospheric air, we use an optical delay line consisting of two rectangular silver mirrors (Fig. 2). The mid-infrared beam makes six 10-m round trips, bouncing off the rectangular mirrors, thus propagating a path of \( L \approx 60 \) m in atmospheric air. The input beam radius in our experiments is \( r_0 \approx 0.7 \) cm, corresponding to a Rayleigh range \( l_R \approx 80 \) m. Spectral measurements in the mid-infrared range are performed with a homebuilt spectrometer consisting of a scanning monochromator and a thermoelectrically cooled HgCdTe detector (Fig. 2). For the spectral measurements in the ultraviolet, visible, and near-infrared ranges, OceanOptics HR4000 and NIRQuest spectrometers were employed.

Figure 2. Experimental setup: GS, grism stretcher; GC, grating compressor; DL, 60-m propagation-path delay line; M1, M2, mirrors.

Transmission over 60 m in atmospheric air gives rise to a dispersion-induced phase shift, readily noticeable in FROG traces (Fig. 3b,d), the spectral phase profiles \( \phi_\lambda(\lambda) \) retrieved from these traces (Fig. 3f,h), and especially in the Wigner spectrograms in Fig. 3) and I. To identify the sign of air GVD within the studied spectral range, measurements with a negatively chirped broadband mid-infrared probe were performed. When transmitted through atmospheric air, such a laser probe is seen to increase its chirp \( \phi \) (cf. Fig. 3k and l). The phase shift across the spectrum of the transmitted pulse (Fig. 3i) is seen to be substantially larger than the change in the phase \( \phi_\lambda(\omega) \) related to the initial chirp of this pulse (Fig. 3k). Correspondingly, the group delay \( \tau_\phi = \partial \phi_\lambda / \partial \omega \) accumulated within the spectrum of the transmitted probe is much larger compared to the group delay \( \tau_0 = \partial \phi_0 / \partial \omega \) related to the initial chirp (cf. Fig. 3k and l).

In Fig. 1d, we present the differential group delay \( \Delta \tau = \tau_\phi - \tau_0 \) which isolates the group delay acquired by the probe due to atmospheric dispersion from the group delay due to the initial chirp. This allows the measurements performed with probe pulses with different initial chirps to be directly compared with each other. The plot in Fig. 1d presents three almost indistinguishable \( \Delta \tau_\lambda(\lambda) \) dependences. Two of these curves represent measurements performed with an almost transform limited (blue line) and negatively chirped (green line) probe pulses. The red line shows the results of calculations performed with the full model of air dispersion including the entire manifold of HITRAN-database infrared transitions. Both the overall behavior of the group delay as a function of the wavelength and the absolute values of \( \Delta \tau_\phi \) achieved in experiments (blue and green lines in Fig. 1d) agree remarkably well with theoretical predictions (red line in Fig. 1d), verifying the predictive power of the model of atmospheric dispersion used in this work. The differential group delay \( \Delta \tau_\phi \) is seen to be a monotonically growing function of the wavelength within the entire wavelength range covered by the spectrum of the laser probe, clearly indicating anomalous GVD within this wavelength range.
Figure 3. (a–d) Measured (a,b) and reconstructed (c,d) FROG traces of the OPCPA output (a,c) and the laser probe transmitted through 60 m in atmospheric air (b,d), (e,f) spectra (solid lines) and spectral phases (dashed lines), (g,h) temporal envelopes (solid lines) and phases (dashed lines) retrieved from the FROG traces of the OPCPA output (e,g) and the laser probe transmitted through 60 m in atmospheric air (f,h), (i,j) Wigner spectrograms of the OPCPA output (i) and the mid-IR laser probe transmitted through 60 m in atmospheric air (j). (k,l) Wigner spectrograms of the mid-IR probe with an initial chirp of $-0.007 \text{ ps}^2$ at the OPCPA output (k) and behind the 60-m delay line (l). The group delay is shown by the dashed line in the Wigner maps.
The absolute values of $\Delta \tau$ achieved in experiments were found to be sensitive to the concentration of CO$_2$ in the room. This observation is consistent with the assignment of negative GVD observed in our experiments to the rovibrational band of atmospheric CO$_2$. To make direct comparison of calculations and experiments possible, the concentration of CO$_2$ in air was measured during the experiment using a standard 7798 CO$_2$ datalogger. With $N_{\text{CO}_2} \approx 1.32 \cdot 10^{16}$ cm$^{-3}$ taken from the readings of the CO$_2$ monitor, calculations are seen to provide a highly accurate fit for the results of $\Delta \tau$ measurements. For this CO$_2$ density, anomalous group delays as long as $\Delta \tau \approx 1.8$ ps are achieved within the wavelength range from 3.70 to 4.15 $\mu$m in our experiments.

Within longer propagation ranges, $L > 60$ m, the laser pulse continues to acquire a group delay due to the anomalous GVD of air. Although the spectrum of our laser probe is close to the CO$_2$ absorption band, it still lies in the region of high atmospheric transmission. At the central wavelength of our laser probe, $\lambda = 3.9 \mu$m, the attenuation length is as long as $L_0 \approx 100$ km. The absorption increases in the long-wavelength tail of the laser pulse, with $L_0 \approx 10$ km at the wavelength $\lambda = 4.17 \mu$m, where the spectral intensity of the laser field is 20 times lower than the maximum intensity at $\lambda = 3.9 \mu$m. As a consequence, even for a propagation range as long as $L = 500$ m, only 4% of an 80-fs, 3.9-$\mu$m transform-limited laser pulse is lost due to atmospheric absorption. In Fig. 4a and b, we show the temporal envelope and the Wigner map of such a pulse calculated for $L = 500$ m using Eqs (3) and (4). The mid-IR probe is seen to acquire a strong chirp within such a long propagation path, which stretches the main peak in the leading edge of this pulse to several picoseconds (the inset in Fig. 4a). The signatures of rotational echo revivals are still observed in the field waveform as weak features at $\tau \approx 120, 175, 225$ and 270 ps (Fig. 4a). In the long-wavelength wing of the laser probe spectrum, the chirp of the pulse is highly nonlinear (Fig. 4b) due to high-order dispersion, which rapidly increases toward the edge of the CO$_2$ absorption band. As long as the peak power $P$ of the laser probe ($P < 50$ GW for laser pulses used in our experiments) is lower than the critical power of self focusing, $P_c \approx 75$ GW at $\lambda \approx 3.9\mu$m, spatial self-action effects do not play any noticeable role in long-range beam dynamics.

The GVD of air is sensitive to the partial density of atmosphere constituent gases. This sensitivity dramatically increases near the absorption bands of the respective gas. A small change in the CO$_2$ density by $\delta N_{\text{CO}_2}$ gives rise to a wavelength-dependent increment in anomalous GVD, which induces a group delay $\delta \tau = c^{-1} \int_0^L [n_1(z) - n_2(z)] dz$ between two spectral components $\lambda_1$ and $\lambda_2$ of a laser probe transmitted over a propagation path $L$, $n_1(z)$ and $n_2(z)$ being the group indices at $\lambda_1$ and $\lambda_2$, which depend on the coordinate $z$ along the propagation path through the local CO$_2$ density $N_{\text{CO}_2}(z)$.

Specifically, for the 80-fs mid-IR laser probe used in our experiments, $\lambda_1$ and $\lambda_2$ can be defined as $\lambda_1 = 3685$ nm and $\lambda_2 = 4140$ nm. Then, taking an average CO$_2$ density $\overline{N_{\text{CO}_2}} \approx 1.32 \cdot 10^{16}$ cm$^{-3}$, as in our experiments, and setting $L$ equal to the minimum of the absorption length $L_0$ within the range of wavelengths from $\lambda_1$ to $\lambda_2$, that is, $L = L_0 \approx 30$ km at $\lambda_1 = 4140$ nm for mid-IR pulses in our studies, we find that a group delay $\delta \tau \approx 80$ fs, which can be reliably detected in the Wigner maps of 80-fs probe pulses, corresponds to an average (over $L$) variation in the CO$_2$ density as small as $\delta N = L^{-1} \int_0^L N_{\text{CO}_2}(z) dz - \overline{N_{\text{CO}_2}} \approx 10^{11}$ cm$^{-3}$, which is equivalent to a sensitivity of 4.7 ppb under normal atmospheric conditions. With the same assumptions, the accuracy of CO$_2$ density measurements that can be achieved with the propagation path $L \approx 60$ m, as in our experiments, is estimated as 2.4 ppm.

To summarize, atmospheric air has been shown to display broadband anomalous GVD in the 3.6–4.2-$\mu$m range, in the high-frequency wing of the asymmetric-stretch CO$_2$ band, that is, in the region where atmospheric air is highly transparent to electromagnetic radiation. Anomalous air GVD demonstrated in this work paves the ways for long-distance signal transmission, new remote sensing techniques, and soliton pulse transformations at high levels of peak powers within long propagation paths in atmospheric air.

Figure 4. Temporal envelope (a) and the Wigner spectrogram (b) of an 80-fs, 3.9-$\mu$m transform-limited laser probe with $r_g \approx 0.7$ cm transmitted through 500 m of atmospheric air calculated with Eqs (3) and (4). The input laser probe is shown by the red line. The group delay $\Delta \tau$ is shown by the dashed line in the Wigner map.
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Author Contributions

A.V.M. contributed to the creation of the mid-infrared source of ultrashort pulses, designed and performed experiments, analyzed the experimental data, participated in filamentation experiment planning and discussions.
A.A.V. designed the study, analyzed the experimental data, performed numerical simulations, contributed to discussions. D.A.S.-B. contributed to the creation of the mid-infrared source of ultrashort pulses, designed and performed experiments, analyzed the experimental data. A.P. contributed to the creation of the mid-infrared source of ultrashort pulses, participated in data analysis and discussions. V.S., E.A.S. and M.V.R. helped perform experiments. S.A. contributed to the creation of the mid-infrared source of ultrashort pulses and participated in discussions. A.B. supervised the creation of the mid-infrared source of ultrashort pulses, contributed to data analysis and discussions. A.M.Z. developed the concept, designed the study, supervised modeling and experiments, analyzed the data, and wrote the paper.

Additional Information

Competing Interests: The authors declare that they have no competing interests.

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