Simulation of Groundwater Movement from Pits Fenced by Zchukovsky's Sprunts

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Abstract

The hydrodynamic production considers the filtration of liquid from the pits, fenced with spools of Zhchukovskiy, through a layer of soil, underrunable by a well-permeable pressure aquifer, on the roof of which contains an impenetrable area. To study infiltration on the free surface of groundwater, a mixed regional multi-parametric task of the theory of analytical functions is formulated, which is solved by the Semibarinova-Kochina method and methods of conformal display of areas of special species characteristic of the tasks of underground hydromechanics. Refs. 24. Il. 4. Table. 1.

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Introduction

Kovsky. In a number of works, free filtration was studied, i.e. the current without support, and in some cases - pressure, i.e. the presence of a free surface was neglected. In all of these studies, infiltration was not recorded. In addition, different techniques were used to solve the problems: the function of Zhchukovsky and the way Vedernikov-Pavlovsky, bringing the case to the conformal display of straight polygons, followed by the use of the Kristoffel-Schwartz formula.[1]

As shown in the "13" way, the practical application of these methods only leads to effective results when the boundary of the area of motion consists of horizontal waterproof and vertical waterproof areas. However, in the real conditions of hydrotechnical construction (channels, reservoirs) directly under cover sediments along with horizontal aquifers of higher permeability (galeks, gravel, coarse-grained sands) are often found and horizontal waterproof areas (impenetrable inclusions, cul-de-pressure rocks), which is fundamentally reflected in the nature of filtration processes. In such situations, the use of Kristoffel-Schwartz integral does not lead to the goal, as in areas of complex flow speed there are already circular polygons that do not boil directly to the straight line.[2]

In contrast to these studies, the following is both a direct continuation and development of the author’s previous works (see. The task of the flow of liquid from the pits through the ground array of finite power, underpowered by a well-permeable pressure aquifer containing a waterproof area on its roof, is studied, if there is infiltration on a free surface. The most common case of movement is considered, in which on both waterproof sections of the border the filtration area the flow takes extreme values and the point of zero flow speed goes to the spool (which, apparently, has not been found in the literature so far). There are extreme cases of current associated with the absence of both support, impenetrable inclusion or infiltration, and the case of degeneration of pits in the semi-endless left flooding strip, previously studied by V. V. Vedernikov. Results are provided for a diagram that occurs in the absence of critical points when the flow rate at the end of the spool is finite; the resulting solution is a certain analogue of the classic task of Zhchukovskiy.[3]

To solve the mixed regional multi-parametric problem, analytical function theory uses the Semibarinova-Kochina method, as well as special-species methods developed for areas of special species, which are very typical of underground hydromechanics. Taking into account the specifics and characteristics of the movement allows you to present solutions through special, and in some cases elementary functions, which makes their application simple and convenient.[4]

On the basis of the built accurate analytical dependencies and through numerical calculations, hydrodynamic analysis of the influence of all physical parameters of the scheme on the picture of the phenomenon is noted and some features of the models being developed are noted. The results of mathematical modeling for all marginal cases are compared to the main filtration scheme. *[5]*

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Main model. Setting a task. The flat established current from A’A through the 2 l-width pit, enclosed by symmetrical S-length sprouts, is considered, through a waterproof layer of T power soil with a substline aquifer E'E containing underground or artesian waters, The pressure in which has a permanent value H_0 (Figure 1).

On the roof of this layer is a waterproof area, D'D simulated horizontal segment length 2L. Due to the symmetry of the motion picture, we will limit ourselves to the study of the right half of the ABCDEGR filtration area.[6]

Groundwater, d flowing ARG spool under the influence of pressure difference in the pit and the underlying well-permeable aquifer, rise behind it to a certain height of the RG and, overcoming the point of zero speed on the spool, form a free surface of GE, which receives infiltration waters with the intensity of e (0<e<1), attributed to the ground filtration factor of the k= const. [7]

We will assume that the movement of groundwater is subject to the law of Darcy with a known filtration factor of z and occurs in a homogeneous and isotropic soil, which is considered...
incompressible.[8]

Under such conditions, as it is known, the basic fluid filtration equations can be recorded as

\[ \varphi = -kh = -k \left( \frac{p}{\gamma} + y \right), \quad \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0, \quad u = \frac{\partial \varphi}{\partial x}, \quad v = \frac{\partial \varphi}{\partial y} \]

...(1)

Where \( \varphi \) is the potential for filtration speed; \( u \) and \( v \) - projections on the axis of filtration rate coordinates; \( h \) - pressure; \( p \) - pressure in the stream; \( \gamma \) is the specific weight of the liquid [9].

From a mathematical point of view, the challenge is to find the complex potential of the flow of \( z \) (\( \varphi \) - the potential of speed, \( \psi \) - the function of the current) as an analytical within the filtration area of the function of the complex coordinates \( z \) under the following boundary conditions:[10]

\[ AB: y = 0, \ \varphi = -H, \ BC: x = 0, \ \psi = 0; \]
\[ CD: y = -T, \ \varphi = 0, \ \psi = Q; \]
\[ DE: y = -T, \ \varphi = -H, \ GE: \ \varphi = -\gamma - T, \ \psi = Q + \varepsilon(x - l), \]

The study is carried out in terms of the values of \( z \) and \( \omega \) which are related to the actual values of the same through the means of equality.[11]

\[ \omega = \frac{w_\varphi}{k}, \quad z = \frac{z_\varphi}{T}. \]

Building a solution to the edge problem. Let’s turn to the area of complex velocity \( w \) (Figure 2) corresponding to the edge conditions (2). This area, which is a circular polygon with three incisions, tops \( M_1 \) and \( N_2 \) two of which correspond to the extremes of current function on impenetrable areas of \( AB \) and \( DE \), belongs to the class of polygons in the polar grids. However, unlike the “15” limit, an additional corner point appears on the boundary of the traffic area, point \( B \) (see Figure 1); the total number of special points becomes nine, making the task much more difficult.[12]

To solve the regional problem, the Semibarin-Kochina method, which is based on the application of the analytical theory of linear differential equations of the Fuchs class. Entered

Auxiliary parametric variable \( \zeta \) and \( z \) functions : conformally displaying the upper half-flatness on the \( z \) area when dots are matched [13]

\[ \zeta = 0, \ \zeta_c = 1, \ \zeta = k^2 \ (0 < k < 1), \ \zeta_0 = \infty, \]
as well as derivatives

\[ \Omega = \frac{d\omega}{d\zeta}, \quad Z = \frac{dz}{d\zeta}. \]

By determining the characteristic performance of the functions of the and the “regular special points” near the regular special points, we will find that they are linear combinations of the two branches of the next function of Riemann.[14]

\[ P \begin{pmatrix} 0 & \zeta_r & 1 & \zeta_1 & \zeta_2 & k^2 & \zeta_5 & \infty & \zeta \cr -1/2 & 2 & 0 & -1/2 & 2 & -1/2 & 0 & 2 & -1 \end{pmatrix} = \]

\[ \frac{Y}{\zeta \sqrt{(1 - \zeta)(\zeta_1 - \zeta)(\zeta_2 - \zeta)(1 - k^2)^2}}, \]

\[ Y = P \begin{pmatrix} 0 & \zeta_r & 1 & \zeta_1 & k^2 & \zeta_5 & \infty & \zeta \cr 1/2 & 2 & 1/2 & 2 & 1/2 & 2 & -1 \end{pmatrix}. \]

...(3)

It can be seen that the points \( \zeta_c = \zeta_1 \) and \( \zeta = \zeta_0 \) are the common points of function \( Y \), representing the last symbol of Riemann, which corresponds to the linear differential equation of the Fuchs class with seven regular special points, very typical for the tasks of underground hydromechanics.[15]

\[ Y''\left( \zeta + \frac{1}{\zeta + 1} + \frac{1}{\zeta - 1} \right) - \left( \frac{1}{\zeta - 1} + \frac{1}{\zeta + 1} + \frac{1}{\zeta - 1} \right) Y' + \frac{3\zeta^2 + 3\zeta + 2}{(\zeta - 1)(\zeta - k^2)(\zeta - k)(\zeta - \zeta_1)(\zeta - \zeta_2)} Y = 0. \]

...(4)

Recall that along with \( \zeta \) the \( \zeta_c \), \( \zeta_0 \) and \( \zeta_0 \) in the equation (4) the accessory parameters of \( f_0 \), \( \lambda_1 \) and \( \lambda_2 \) remain unknown in setting the task and must be determined in the course of its solution.

Replacing variables

\[ \zeta = \text{sn}^2(2K\tau,k) \]

translates the upper half-flatness \( \zeta \) into a rectangle of the plane:

\[ 1/2 \quad 0 < \tau < 1/2 \quad (k) = K / K, \quad K = K(k), k' = \sqrt{1 - k^2} \]

I’m where \( \rho \), \( K(k) \) is a full elliptical integral of the first kind with module \( k, \ 23, \) when dots are
Figure 1. A picture of the current from the pit, calculated at the $e = 0.6$, $T = 7$, $S = 3$, $H_0 = 3$, $L = 15$, $H = 4$, $l = 10$

Figure 2. Complex $W$ speed area for the main filtration scheme
matched
\[ \tau_E = 0, \quad \tau_G = 1/2, \quad \tau_C = 1 + \frac{i\rho}{2}, \quad \tau_D = \frac{i\rho}{2}, \]
and the \( Y \) equation integrals (4), which correspond to the symbol of Riemann (3) and are constructed according to the technique developed earlier, are transformed as follows:
\[ Y_{1,2}(\tau) = B_0^{-1}(\tau)B_1(\tau \pm i\beta)B_2(\tau \pm i\beta)\exp(\pm i\pi). \quad (6) \]
Here, \( \tau = \arcsn (u, k) \) is Jacobi’s elliptical function (sinus) at module \( k \), \( B_i(q) \) - theta function with the parameter \( q \) exp, which is uniquely associated with the module \( k, q, \gamma \) - some suitable permanent.[16]

Taking into account the ratios (3), (5) and (6), as well as the fact that the functions has the same appearance.
\[ w = i\sqrt{\varepsilon}x^1(\tau) = (1 + \sqrt{\varepsilon})Y_1(\tau) \pm (1 - \sqrt{\varepsilon})Y_2(\tau), \quad \varepsilon = \sqrt{\varepsilon}, \quad \theta(\rho/2 + \beta - \alpha - \gamma), \quad (7) \]
come to the additions we’re in.
\[ \Omega = -\sqrt{\varepsilon}N x^1(\tau) \Delta(\tau), \quad Z = i\sqrt{\varepsilon}x^1(\tau) \Delta(\tau), \quad \Delta(\tau) = \sin(2K\tau, k)\sqrt{1 - (1 - k^2A^2)\sin^2(2K\tau, k)[1 - (1 - k^2B^2)\sin^2(2K\tau, k)]} \]
\[ \quad \Delta(\tau) = \sin(2K\tau, k)\sqrt{1 - (1 - k^2A^2)\sin^2(2K\tau, k)[1 - (1 - k^2B^2)\sin^2(2K\tau, k)]} \quad (9) \]
in which \( N \) is a large-scale constant simulation, \( A = \arcsn (2Ka, k) \), \( B = \arcsn (2Kb, k) \), \( a \) and \( b \) unknown residents of points \( A \) and \( B \) of the area of \( q \).

(9) Permanent conformal displays of \( q, z \) and \( y \), which are bound by a ratio (8), are subject to the conditions
\[ 0 < a < r < b < m < a < b < \rho/2, \quad 0 < y < \rho/2, \]
\[ \quad (10) \]
Regulating the position on the boundary of the flow of points \( M \) and point of the spun \( R \), as well as \( N_1 \) and \( N_2 \); \( m \) and \( r \) are unknown residents of \( M \) and \( R \) points in the plane. \( \tau \). You can verify that the functions (9) meet the conditions (2) reformulated in terms of \( \text{functions} \), and thus are a parametric solution to the original edge problem.[17]

Recording ratios (9) for different parts of the boundary of the area, followed by integration across the entire loop of the auxiliary area, leading to a close of the movement area and thus serves as a control of the calculations.[18]
\[ \int_a^b Y_{BA} dt = S, \quad \int_a^b X_{AB} dt = l, \quad \int_0^{1/2} X_{CD} dt = L, \quad \int_0^{\rho/2} Y_{BC} dt = T, \]
\[ \quad (11) \]
\[ \int_0^{\rho/2} \Phi_{BC} dt - \int_0^{1/2} \Phi_{CD} dt = H - H_0, \quad (12) \]
\[ d = T - H_0 - \int_a^b \Phi_{EG} dt, \quad Q = \int_a^b \Psi_{BC} dt \]
\[ \quad (13) \]
\[ \text{Account control is other expressions for the values} \ d, L \text{ and filtration} \ \text{expense:} \]
\[ \int_0^{1/2} Y_{EG} dt = d + \int_0^{1/2} Y_{EG} dt, \quad 0 \leq u \leq 1/2 \]
\[ \quad (14) \]
In formulas (11)-(14) subtegrial functions are expressions of the right parts of equality (9) on the corresponding sections of the contour of the region.[19]

Analysis of numerical results for the main filtration model. Views (9) --(14) contain seven unknown permentals: residency prototypes of points \( A, B, R \) in the plane \( \tau \), parameters of conformal display, \( \gamma \), satisfying ratio (8) and inequities (10), as well as module \( k \) \( 0 < k < 1 \) and constant \( N \) modeling. \( N \)
\[ w^{-1}(1/2 + ir) = 0, \quad \int_0^{1/2} (\Phi_{EG} + \Phi_{CD}) dt + \int_0^{1/2} \Phi_{GA} dt + \int_0^{\rho/2} \Phi_{BC} dt = 0 \]
The first means that the speed at the end of the spool turns into infinity, and the second is directly...
derived from the consideration of boundary conditions (2). After determining the unknown permanents are the exact values \( d \) and \( z \) by expressions (12) and finally, the formulas (13) are calculated coordinates of the points of the free surface \( EG \).[20]

On rice. 1 is a picture of the current, calculated at \( q = 0 \). 6, \( T_0 = 7, S,H = 3, H \). 3, \( L = 15, H, = 7L, 10 \) (basic values), and the rest are fixed by the baseline values, the results of calculations of the influence of the determining physical parameters are \( 0, T,S,H \) and \( L \) on the depth of \( D \) (negative values \( d \) means that the free surface rises above the abiss axis) and the expense of the \( q \). Figure 3 are represented by the dependence of the \( d \) and filtration consumption of the \( 0,T,H,H,H,H,L,H. H.\). \( \varepsilon, T,S,H \) and \( L,H,l \).[21]

Analysis of table and rice data. 3, and allows you to draw the following conclusions.

First of all, the same quality of dependencies of the values \( H, L, d,S \) and \( l \), associated with a decrease \( Q \) infiltration intensity and greater reservoir power, in which these filtration characteristics grow.[22]

Increase infiltration intensity, impenetrable inclusion and pressure in the underlying layer and reduce the power of the layer, The length of the spool, the \( d \) pressure of the water in the pit \( \varepsilon,S,H \) and its width lead to a drop in the depth \( d \), i.e. to the increase of the residents of the point \( G \) exit of the depression curve from under the spool.[23]. Table 1.

The results of the calculations of \( D \) and \( Z \) values. However, the greatest impact on the depth of \( D \) is an impenetrable area: table data show that when \( L \) width increases by only 28%, the depth \( d \) increases by almost 10 times.

At \( d = (−d)S, H(S) = 0 \). \( H, \varepsilon,T,S,H_0,L,H,l \). \( H \)

0.8, \( H \) and 5 and \( L \) and \( L \) 18, i.e. at fairly large parameters, \( H,H_0 \) and \( L \), the free surface rises above the abscissus axis, with the values \( d \) negative. Tab 2.

characterizing the relative elevation of groundwater behind the spool, \( \varepsilon,H \) we receive \( h=(−1) \). ( 1945) = 1. 3981, \( H=−0. 9297 \) = 1. 3099, \( H=−2. 3500 \) = 1. 7833 and \( H=−0. 2560 \) = 1. 0853, with the parameter \( h \) grows with \( T,H_0 \) an increase in the residents of point \( G \) exit of the depression curve from under the spool. [24]

As for the flow, the larger the width of the impenetrable inclusion, the more significant the difference in the value of \( \text{theq} \) : from the table it follows that when the \( L \) parameter grows by 1.28 times the expense increases by more than 12 times.

This behavior of consumption is clearly seen both with the increase in the power of the layer, the width of the pit and the pressure in the underlying horizon, and with the decrease in the length of the spool and the pressure in the beef. It follows from the table that the reduction of the \( H \) parameter by only 2 times is accompanied by an increase in consumption of almost 48 times, which indicates the greatest impact on the pressure of water in the pit.

Limit cases. 1. Case \( H_0 \) \( q \) 0. We will focus primarily on the absence of backup, i.e. movement at \( H_0 \) \( q \) 0 . The solution for it is derived from dependencies (9)-(14) at the \( y=\gamma=\gamma^* \) 0. At this value of they circular incision of the \( EG \) area \( w \), transforming, transforming, degenerates into the right semicircle (bar line on Figure 2), and thus the original area becomes a circular hexagon, which falls the right part of the semicircle . \( w=\sqrt{(1+\epsilon/2)} \) \( (1−\epsilon)/2 \ln \) the \( z \) current plane at the \( \gamma=\gamma^* \) the depression curve is rinsed at \( E \) point, \( E \) with which its inflection point \( F \) merges, and overlooks the roof of the underlying horizon at right angles.

Note that for \( q \) 0. 7, \( T \) 6 and 6.. 5, \( S \) \( q \) 3, \( L \) \( q \) 15, \( H \) \( q \) 5 and \( l \) \( q \) 10, in which the value of \( D \) becomes negative, the \( H \) is 1.2191, 1.2020, 1.0140, 1.0443, 1.0638 and 1.0442 respectively.

Case = 1

\( Z' = Z + b \rho/2 \) \( A \) \( b \) \( b \) \( \rho \). Consider the case where the width of \( * \) \( \infty \) the pit increases indefinitely, so that the filtration area becomes a semi-endless flooding band on the left.

In 0th main filtration scheme discussed above, the absence of such a powerful factor as impenetrable inclusion, being the limit, serves as a backdrop to assess the role of infiltration and pressure in the underlying layer and allows for a more contrasting response to the interaction of such important physical parameters as \( q \) and \( H_0 \).

If there is no impenetrable area on the roof of
Figure 3. Dependencies of values $d$ (1) and $q$ (2) from different parameters (a - from $T$ at $H_0$, $S$, 3, $H_0$, 3, $L$, 15, $H$, 7, $d$ at 10; b - from $T$ at $H_0$, $S$, 3, $H$, 7, $d$ at 10; c - from $S$ at 0.6, $T$, 0.6, $H_0$, 3, $L$, 15, $H$, 7, $d$ at 10; d - from $S$ at 0.6, $T$, 0.7, $L$, 15, $S$, 3, $H$, 7, $d$ at 10; e - from $H$ at 0.6, $T$, 0.7, $S$, 3, $H_0$, 3, $L$, 15, $d$ at 10; f - from $l$ at 0.6, $T$, 0.7, $S$, 3, $H_0$, 3, $L$, 15, $d$ at 10).
Table 1.

| E  | D    | Q   | T  | D    | Q   | S  | D    | Q   | H0 | D    | Q   |
|----|------|-----|----|------|-----|----|------|-----|----|------|-----|
| 0.5| 2.651| 0.182| 6.5| 1.349| 0.234| 2.0| 1.726| 0.635| 2.0| 3.155| 0.038|
| 0.6| 1.804| 0.394| 7.0| 1.804| 0.394| 2.5| 1.745| 0.563| 4.0| 0.441| 0.769|
| 0.7| 0.586| 0.457| 7.5| 2.299| 0.457| 3.5| 1.844| 0.255| 5.0| -0.93 | 1.159|
| 0.8| -1.195| 0.094| 8.0| 2.745| 0.627| 4.0| 1.873| 0.129| 6.0| -2.35 | 1.815|

Table 2.

| L  | D    | Q   | H  | D    | Q   | L  | D    | Q   |
|----|------|-----|----|------|-----|----|------|-----|
| 14 | 2.555| 0.086| 4.0| 0.650| 1.815| 10.0| 1.804| 0.394|
| 16 | 1.116| 0.599| 5.0| 1.070| 1.159| 10.3| 2.018| 0.320|
| 17 | 0.413| 0.888| 6.0| 1.441| 0.769| 10.6| 2.229| 0.253|
| 18 | -0.256| 1.084| 8.0| 2.155| 0.038| 11.0| 2.478| 0.230|

Figure 4. The current pattern in the case of \( \nu \in \mathbb{R} \), calculated at 0.5, \( T'q 6, S'3, H_0'q 0 \), 
\( L = 16.2, H = 3.8, l = 15 \)
the underlying aquifer, the latter becomes well permeable all along. When $1/2 \text{ Im Re } D C$ and $D$ points merge in the area of complex speed, $C w$, its left semi-flatness is cut off, The circular incision of the EG goes into the right half-flatness, and the original area is transformed into a $\infty$ circular triangle.

$$\rho = K'/K = \infty, \quad K = \pi/2.$$  

The solution for this extreme case is derived from formulas (9)-(14), if they put $k q 0$ and take into account that in this case elliptical functions degenerate into trigonometry, and theta functions break off on their first members or constants:

$$\Omega = -\varepsilon N \sin 2\theta' \sin 2(\tau - m'), \quad Z = i N \sin 2(\tau - r') \cos \Delta(\tau),$$  

$$\Delta(\tau) = \sqrt{(\alpha - \sin^2(\theta)(b - \sin^2(\tau)(c - \sin^2(\tau)), \quad \tau = i g2\alpha\varepsilon c2l', \quad m' = \arcsin \sqrt{m}, \quad r' = \arcsin \sqrt{r}, \quad m', r', c'(0 < m' < \theta' < a' < b' < c' < \pi/2);$$

where $m' = 0$ case of $= 0 L$, we will focus on the absence of infiltration.

Thus, it turns out to solve the problem, first considered by V. V. Vedernikov, only in another way.

A case of the final speed of the flow at the end of the spool. As part of the edge task (2), consider the case where the flow rate at the end of the spool $\nu_0 < e$ $0 q t$: Then in the area of complex speed $w$ both vertical incisions disappear, the left half-flat is cut off, as before at $L q 0$, however, unlike the latter, the MR section is transferred to the first quadrant.

The parametric solution of the problem formally has the same form (9) with the replacement of integrals $Y_{1,2}(q)$ and permanent conformal display of $q$ and $q$ for the following:

$$Y_{1,2}(\tau) = \theta^{-1}(\tau) J_1 \theta(\tau \pm i \varepsilon) \exp \pm int\tau, \quad (16)$$

$$a = \beta = (1 + i \varepsilon) / 2. \quad (17)$$

The solution to a similar problem in the absence of backup arises from submissions (9), (16), (17) at $y$ of $y^*$.  

Analysis of the numerical results shows that in $\nu_0 q t$: the qualitative nature of filtering dependence on the physical parameters of the scheme is maintained, characteristic of the case $\nu_0 \infty$. For example, there is the same as before, the pattern of flow behavior from values $T$ and $l$, on the one hand, and contrary to the parameters of $S$ and $H$, on the other.

On rice. 4 is a picture of the movement, calculated at the $z 0.5, T = 6, S = 3, H = 0, L = 16, 2, H = 3, 8, l = 15$. It is noteworthy that for all the calculated variants $1)$ of $d s$ and therefore $h(d)$ $h(s) q 0$. This means that in the current plane point $G$ exit of the depression curve from under the spool merges with the point $R$ of its edge; from the consideration of the area of complex speed $w$ it follows that in this case the speed at the end of the spint is equal to the intensity of the infiltration: $\nu_q$ (Figure 4).

If you make a transformation $T' = 1/2 + i \varepsilon l$ that translates a rectangle of auxiliary variables to a similar one to the parameter, then the corresponding basic filtering scheme of the inequality to the parameters (10) will take the form

$$0 < b' < a' < r' < 1/2;$$

Where $b', a' < r'$ there are abscisses of $B, A, R$ points in the plane.

Calculations show that for any infiltration intensity, the $d > S$, ratio $d S$ is only for $r'$ a single $R$ - its limit - when the $G R$: $r' = r' = 1/2$ plane $r' < r'$ is merged.

Such a result in the marginal case for the model in question, when the waterproof layer of soil has unlimited power, there is no impenetrable site and infiltration, i.e. at the time of

$$T = \infty (k' = 0, k = 1), \quad L = 0 (b' = b' = 0);$$

$1 And $\varepsilon = 0 (m' = 0)$, was first received by N. E. Schukovsky.

$$K = \infty, \quad K' = \pi/2, \quad k' = 0, \quad k = 1, \quad b' = 0, \quad q' = 0,$$

and we can be sure that it is valid.
3. Thus, in the extreme case of the scheme studied, it turns out to solve the problem of Shchukovsky, but only in a different way.

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