1. Introduction

The paper investigated different electric motors used in variable speed drives. It is in these drives only that it is worthwhile to use dc motors with an electronic or mechanical commutator. The variable speed drives are used in the following cases:

- when changes in speed are required by the duty algorithm of the drive (e.g. roll mill drive),
- when the drive should operate at minimum energy consumption – energy-saving drive.

Energy-saving drives are preferable from the viewpoint of environmental protection.

Energy-saving operation is achieved when the drive is run at minimum speed compatible with the requirements of the engineering process.

Variable speed drives can be equipped with the following motor types (Fig 1):

- **dc motor** (Ma) with electromagnetic excitation supplied from a power electronics converter (rectifier) ac/dc,
- **dc motor** (Mb) excited by permanent magnets (NdFeB) placed in the stator supplied from a power electronics converter (rectifier) ac/dc,
- cage induction **motor** (Mc) supplied from a power electronics converter (inverter) ac/dc/ac,
- asynchronous cascade consisting of slip-ring induction **motor** (Md) and inverter/transformer set used for transmitting electrical energy from the rotor to the power network,
- **brushless motor** (Me) excited with permanent magnets (NdFeB) placed in the rotor supplied from power electronics circuit called an electronic commutator ac/dc/ac.

**Fig 1.** Different drive systems:

a – dc motor with electromagnetic excitation; b – dc motor with PM excitation; c – cage induction motor; d – asynchronous cascade; e – brushless motor with PM excitation
The comparison of the rated power and efficiency of these motors is given in the paper. The comparison criteria are:

- external overall dimensions \( D = 400 \) mm, \( l = 660 \) mm (Fig 2),
- identical cooling system (forced ventilation).

Dc motor with electromagnetic excitation (Ma) has been manufactured in Poland for more than 30 years. It is used in 105N trams drive. Its ratings are: \( P_N = 40 \) kW; \( V = 300 \) V; \( I = 150 \) A; \( n = 1800 \) rpm; efficiency 89%.

The power losses under nominal operating conditions are \( \Delta P = 4940 \) W. These losses can be divided into:

- excitation winding losses \( \Delta P_f = 747 \) W,
- armature winding losses \( \Delta P_a = 3200 \) W,
- iron losses \( \Delta P_{Fe} = 673 \) W,
- mechanical losses \( \Delta P_m = 320 \) W.

Rotor diameter \( D_a = 220 \) mm; rotor active length \( l_a = 220 \) mm; rotor volume \( V_a = 8.36 \) dm³.

Dc motor with PM excitation (Mb) (Fig 3) has been constructed by modifying motor existing design. Permanent magnets (NdFeB) have been glued to the pole shoes on the air gap side.

The excitation pole arc length of Mb motor has been assumed to be the same as in Ma motor \( b_a = b_b = 115 \) mm and commutation winding parameters have also been left unchanged. Indexes “a” and “b” relate to Ma and Mb motors, respectively. Since excitation winding is absent in Mb motor, the window cross-section between the main poles and commutation poles may be decreased, since this window contains commutation poles winding only.

Hence, rotor diameter of Mb motor can be increased. The rated power \( P_{N_b} \) of Mb motor can be estimated from the formula [1]:

\[
P_{N_b} = P_{N_a} \left( \frac{V_a}{V_b} \right)^{3/4}.
\]  

(1)

Diameter \( D_b \) of the new motor will be greater, since the window cross-section between the main poles and commutation poles will be decreased. In Ma motor excitation coil two flat copper wires are placed near the pole. The height and width of these wires are \( a = 1.3 \) mm, \( b = 20 \) mm. A window in a new motor can be reduced in the radial direction by one wire width (b) less radial length of PM (\( l_m \)), or (\( b - l_m \)) altogether.
Maintaining the air gap induction and assuming that air gap width is equal to $\delta_b = 2 \text{ mm}$ (in $Ma$ motor the air gap is equal to $\delta_a = 3 \text{ mm}$), NdFeB PM length should be equal to $l_m = 6 \text{ mm}$. This is determined by calculating the induction at rotor surface when a magnetic circuit is excited with permanent magnets [2].

$Mb$ motor rotor diameter and rotor volume will therefore be equal to:

$$D_b = D_a + 2 \cdot (b - l_m + \delta_a - \delta_b),$$

$$V_b = \frac{\pi}{4} D_b^2 \cdot l.$$  

$Mb$ motor rated power at continuous duty (51) is determined by equation (1). Its rating is $P_{Nb} = 56 \text{ kW}$.

$Mb$ motor efficiency will go up, since excitation losses $\Delta P_{f_e}$ are non-existent. The power losses in the main poles pole shoes will also be less, since the air gap for alternating components of the flux will be increased from $\delta_a = 3 \text{ mm}$ to $\delta_b + l_m = 8 \text{ mm}$. These losses are due to:

- slot pulsations of excitation magnetic flux,
- armature reaction flux pulsations due to power electronics converter.

These losses are neglected in the overall power balance.

Armature power losses in $Mb$ motor will increase in proportion to rotor volume:

$$\Delta P = (\Delta P - \Delta P_{f_e}) \cdot \frac{V_b}{V_a}.$$  

These losses ($\Delta P = 5416 \text{ W}$) are greater than total power losses in $Ma$ motor. In order to keep the motor heat balance, total losses should not exceed 4940 W (value for $Ma$ motor). This can be achieved by decreasing $Mb$ motor rated power $P_{Nb}$ by 5 %, i.e. from 56 kW to 53 kW. The power losses will go down to $\Delta P = 4852 \text{ W}$.

$Mb$ motor efficiency is equal to:

$$\eta = \frac{P_{Nb} \cdot 100}{P_{Nb} + \Delta P}.$$  

Efficiency is determined by equation (5). Its rating is $\eta = 91.6 \text{ %}$.

To summarize, using the casing of $Ma$ motor it is possible to design $Mb$ motor with greater rated power and with higher efficiency.

$Dc$ motor $Mb$ excited with NdFeB permanent magnets will be a separately excited motor with one speed control range at constant torque.

$Ma$ and $Mb$ motors characteristics are presented in Table.

3. Cage induction motor $Mc$

Cage induction motor $Mc$ has been designed by the authors with identical dimensions as $Ma$ motor and is currently being manufactured and employed as the main drive motor for 105N N type trams. It is often installed in the tram during vehicle general overhaul, when the drive is modernized. Since there is no commutator, the active part of the winding is longer (i.e. stacking is longer) $l_c = 300 \text{ mm}$. Inner stator diameter is equal to $D_b = 215 \text{ mm}$. Inner rotor volume $V_c = 10.9 \text{ dm}^3$ is almost the same as in $Mb$ motor. Rated power of $Mc$ motor is identical as in $Mb$ motor and equal to $P_{Nc} = 53 \text{ kW}$.

Power losses in $Mc$ motor are determined on the basis of a motor test report (conducted by the manufacturer).

The rated parameters are: $P_{Nc} = 53 \text{ kW}$; $U_n = 380 \text{ V}; 60 \text{ Hz}; I_{1N} = 91.6 \text{ A}$. [3].

Power losses are as follows:

- iron losses $\Delta P_{Fe} = 600 \text{ W}$,
- armature winding losses $\Delta P_{al} = 1900 \text{ W}$,
- rotor winding losses $\Delta P_{ml} = 2090 \text{ W}$,
- mechanical losses $\Delta P_m = 170 \text{ W}$.

The power losses of $Mc$ motor under rated operating conditions are $\Delta P_N = 4760 \text{ W}$.

$Mc$ motor rated efficiency is determined as well as $Mb$ motor. Its rating is $\eta = 91.7 \text{ %}$.

Power factor is equal to:

$$\cos \varphi_N = \frac{P_{Nc}}{\sqrt{3} \cdot U \cdot I}.$$  

Power factor is determined by equation (6). Its rating is $\cos \varphi_N = 0.88$.

The induction motor with scalar control can operate in two speed control ranges, i.e. constant torque range, then $l_d = l_a = 220 \text{ mm}$ and constant power range, then $n_N \leq n \leq n_{max}$.

However, usually vector control is used since it improves the drive dynamics and brings it close to $dc$ motors dynamic properties.

$Mc$ motors characteristics are presented in Table.

4. Asynchronous cascade $Md$

Asynchronous cascade consists of a slip-ring induction $Md$ motor and a frequency converter ac/dc/ac connected into rotor circuit – see Fig 1.

The active length of $Md$ motor will be similar (identical) to that of $Ma$ motor $l_d = l_a = 220 \text{ mm}$, since slip rings take up the place allotted to the commutator in $Ma$ motor. The inner stator diameter $D = 215 \text{ mm}$ will be the same as in $Mc$ motor.

The rated power of $Md$ motor will be less than
that of Mc motor. Roughly, it will decrease in proportion to length ratio \( \frac{l_d}{l_c} \), since the diameter \( D_d = D_c \):

\[ P_{Nd} = P_{Nc} \frac{l_d}{l_c}. \]  

(7)

Rated power is determined by equation (7). It rating is \( P_{Nd} = 38.8 \text{ kW} \).

Iron losses, while induction remains the same, will also decrease by the same ratio \( \frac{l_d}{l_c} \). Its rating is \( P_{Fe} = 440 \text{ W} \).

Armature winding copper weight will be less by 8%, since the end windings in Mc and Md motors are identical. Mechanical losses will decrease at the same rate and their rating is \( P_{dm} = 1748 \text{ W} \).

The rotor winding losses will not change, since even though the losses in the active parts of the winding fall down by 17%, the losses in the end windings will rise as well as the losses in the slip-ring head. Therefore it has been assumed that \( P_{dm} = 2090 \text{ W} \).

The mechanical losses will increase \( \Delta P_{md} = 320 \text{ W} \).

Total power losses in Md motor at rated power are equal to \( P_{Nd} = 4598 \text{ W} \).

However, if the cooling factor is considered, the power losses may be increased up to \( \Delta P_{Nd} = 4760 \text{ W} \), and then the rated power will also go up by ratio 4760/4989 and is equal \( \Delta P_{Nd} = 40 \text{ kW} \).

Md motor rated efficiency is determined as well as Mb motor. Its rating is \( \eta = 89.4 \% \).

The reactive power of Md motor will be less than the reactive power of Mc motor, approximately proportionately to the active length:

\[ Q_d = Q_c \frac{l_d}{l_c}, \]  

(8)

\[ Q_c = \frac{P_{Nc}}{\eta_c} \sin \varphi_c. \]  

(9)

Taken into consideration equations (8) and (9) \( Q_d = 20 \text{ kVAr} \).

Md motor power factor is:

\[ \cos \varphi_d = \frac{R_{Nc}}{\sqrt{R_{Nc}^2 + Q_d^2}}, \]  

(10)

\[ R_{Nc} = P_{Nc} + \Delta P_{Nc}. \]  

(11)

Power factor is determined by equation (10) and (11). Its rating is \( \cos \varphi_d = 0.91 \).

Md motors rated parameters: voltage \( U_N = 380 \text{ V} \); 60 Hz; current flowing

\[ I_N = \frac{P_{Nc}}{\sqrt{3} \cdot U_N \cdot \cos \varphi_d} = 74.7 \text{ A}. \]

Md motors characteristics are presented in Table.

5. Dc brushless motor Me excited with permanent magnets

The magnetic circuit of brushless Me motor with electronic commutator is shown in Fig 4.

Motor stator and stator windings are identical as in the induction Mc motor. The stacking length may remain unchanged and equal to \( l_e = 300 \text{ mm} \) and the stator inner diameter may be equal to \( D_e = 215 \text{ mm} \). It has also been assumed that air gap \( \delta_e = 1 \text{ mm} \) and magnetic length of permanent magnets \( l_m = 4 \text{ mm} \). The brushless Me motor with an electronic commutator, at load power 53 kW (continuous duty 51) will be characterised by better operating parameters than an induction motor [2].

Current flowing in the winding will possess the active component only:

\[ I_A = I_{An} \cdot \cos \varphi_c. \]  

(12)

Me motor current flowing is determined by equation (12). Its rating is \( I^*_{An} = 80.6 \text{ A} \).

Active power losses in the motor can be calculated from the formula:

\[ \Delta P = \Delta P_{Fe} + \Delta P_{m} + \Delta P_{d} \]  

(13)

since power losses in the rotor and power losses in the stator winding caused by a current passive component are nil:

\[ \Delta P = \Delta P_{Fe} + \Delta P_{m} \cdot \cos \varphi_c^2. \]  

(14)

Me motor power losses are determined by equation (14). Its rating is \( \Delta P = 2241 \text{ W} \).

Md motor efficiency rises up to \( \eta = 95.9 \% \).

The efficiency of a brushless Me motor with an electronic commutator is higher by 4.2% than the
Specification of basic parameters of motors intended for 105N tram drive

| No | Parameters | Motor type |
|----|------------|------------|
|    |            | Ma         | Mb         | Mc         | Md         | Me         |
| 1  | Rated power for continuous duty (SI), kW | 40 | 53 | 53 | 40 | 53 | 77 |
| 2  | Rated voltage, V | 300 | 300 | 380 | 380 | 380 | 380 |
| 3  | Input power, kW | 44.94 | 57.84 | 57.76 | 44.76 | 55.24 | 81.76 |
| 4  | Power losses, W | 4940 | 4842 | 4760 | 47.60 | 2241 | 4760 |
| 5  | Efficiency, % | 89 | 91.6 | 91.7 | 89.4 | 95.9 | 94.1 |

induction motor efficiency. However, if it is assumed that the heat exchange is identical as in Mc motor, then power losses can be increased up to $\Delta P = 4760$ W, and rated power subsequently increases up to $P = 77$ kW.

Hence a brushless Me motor with an electronic commutator can be designed on the basis of Ma motor dimensions. This new motor will be excited with permanent NdFeB magnets and it will be rated at 77 kW. Its rated efficiency is determined and its rating is $\eta = 94.1\%$.

This motor type makes possible the achievement of the highest power and efficiency at the given volume. The motor operates as a dc motor excited with permanent magnets, i.e. only one range of speed control is available ( $T = \text{const}$ ); the speed varies as supply voltage changes.

This motor is also characterised by high torque overload capacity depending on allowable transistor currents and mechanical strength of the shaft, coupling and transmission.

Me motors characteristics are presented in Table.

6. Recapitulation

Table sets out characteristic parameters of 5 different Ma–Me motor types, all designed with the same external dimensions as shown in Fig 4.

7. Conclusions

- Variable speed drives can be designed with five different motor types shown in Fig 1.
- The brushless Me motor with an electronic commutator excited with permanent magnets is characterised by the best operational parameters. For the given motor volume the rated power and efficiency are the highest.
- The brushless motor with an electronic commutator is as reliable as a cage induction motor since there are no movable contacts, there are no active power losses in the rotor. It ensures the highest overload capacity of all the investigated motors.

References

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