Near-infra-red spectroscopic ages of massive star clusters in M 82

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ABSTRACT

Context. Like other starburst galaxies, M 82 hosts compact, massive (>5 × 105$M_\odot$) young star clusters that are interesting both in their own right and as benchmarks for population synthesis models.

Aims. In addition to assessing or reassessing the properties of some of the brightest near-IR sources in M 82, this paper addresses the following questions. Can population synthesis models at $\lambda/\delta\lambda \approx 750$ adequately reproduce the near-IR spectral features and the energy distribution of these clusters between 0.8 and 2.4 μm? How do the derived cluster properties compare with previous results from optical studies?

Methods. We analyse the spectra of 5 massive clusters in M 82, using data acquired with the spectrograph SpeX on the InfraRed Telescope Facility (NASA/IRTF) and a new population synthesis tool with a highly improved near-IR extension, based on a recent collection of empirical and theoretical spectra of red supergiant stars.

Results. We obtain excellent fits across the near-IR with models at quasi-solar metallicity and a solar neighbourhood extinction law.

Conclusions. The observed IR-bright clusters are part of the most recent episode of extended star formation in M 82. The near-IR study of clusters that are too faint for optical observation adds important elements to the age distribution of massive clusters in dusty starbursts. Further joint optical and near-IR spectroscopic studies will provide strong constraints on the uncertain physics of massive stars on which population synthesis models rest.

Key words. galaxies: individual: M 82 – galaxies: star clusters – galaxies: stellar content – galaxies: starburst – infrared: galaxies – stars: supergiants

1. Introduction

Starburst galaxies host large populations of star clusters, and it has become increasingly clear that global star formation processes and cluster formation processes are intimately linked (Meurer et al. 1995; Larsen 2006; Elmegreen 2006). This is an important motivation for detailed studies of young star clusters, their distributions in terms of mass and age, their mass-to-light ratios and their stellar initial mass functions.

Because star formation originates in molecular clouds, starburst galaxies tend to be dusty, and young star clusters can be severely obscured. As beautifully illustrated by near-IR and optical Hubble Space Telescope (HST) images of galaxies such as M 82 or the Antennae (de Grijs et al. 2001; Alonso-Herrero et al. 2003; McCrady et al. 2003; Rossa et al. 2007), the brightest near-IR star clusters can go undetected at optical wavelengths, and vice-versa. Optical studies tend to focus on lines of sight through holes in the dust, and the derived distributions of cluster properties are subject to biases. In order to obtain a more complete picture of the cluster populations, it seems crucial to combine optical and near-IR data. This can be done with multi-band photometry or with spectroscopy.

The importance of near-IR spectroscopy in studies of dusty star forming galaxies has long been recognised (Rieke & Lebofsky 1979), and spectra in the H or K windows have been used to constrain star formation histories (e.g. Rieke et al. 1993; Oliva et al. 1995; Lançon & Rocca-Volmerange 1996; Satyapal et al. 1997; Förster Schreiber et al. 2001).

However, near-IR studies of young stellar populations remain difficult. Among the relevant problems are the following (see main text for details and references).

(i) Evolutionary tracks for massive stars are uncertain, in particular in the red supergiant phase which is the predominant source of near-IR light at ages of order 107 yr.

(ii) Model atmospheres for luminous red supergiants are not yet reliable, and this affects the mapping of isochrones into colour diagrams.
(iii) The stellar population of a cluster is stochastic, and the intrinsically small number of bright stars leads to potentially large spreads and systematics in the expected cluster properties.

(iv) The subtraction of very irregular starburst galaxy backgrounds can be hazardous.

(v) It matters to photometric studies that the shape of the dust attenuation law depends on the unknown spatial distribution of the dust as well as on the nature of the dust; there are degeneracies in colours, for instance between age and extinction.

As a result of some or all of the above, discrepancies between photometric studies that do or do not include near-IR passbands can occur. The consistency between results obtained from near-IR and from optical spectroscopic data needs to be tested.

With extended spectroscopy of massive star clusters, by which we mean spectroscopy that extends through optical and near-IR wavelengths, it becomes possible to isolate some of the above aspects. By using stellar absorption features exclusively, dust attenuation issues are mostly eliminated. By focusing on very massive star clusters, stochastic effects can be kept below acceptable levels. Contamination by other stellar populations on neighbouring lines of sight remains an issue in crowded areas, but can be addressed with multicomponent models, more safely with spectroscopy than with photometry. In the end, the spectroscopic analysis is mostly sensitive to the ingredients of the population synthesis models, such as the stellar evolution tracks and the stellar spectra assigned to each point along these tracks. One may expect two types of results. If the best-fit models based on the near-IR data are not consistent with the optical data, this points to inadequacies of the input physics of the models, i.e. likely systematic errors in both optical and near-IR cluster ages. Conversely, a good fit to the optical and near-IR data set will provide significantly more robust cluster properties than a fit to a single spectral window or to photometric data.

In this paper, we analyse extended spectra of five massive clusters in the nearby starburst galaxy M 82, using a population synthesis tool with a highly improved near-IR spectroscopic extension. We show that it is possible to obtain a good representation of all the near-IR features (0.8 \( \mu \)m to 2.4 \( \mu \)m). We allowed Mouhcine & Lançon (2002) and Maraston (2005) to produce extended synthetic single stellar population spectra (SSP spectra) with a near-IR resolution \( R = \lambda/\delta \lambda \sim 1000 \). That work focused on intermediate age populations, in which O-rich and C-rich TP-AGB stars are the predominant sources of near-IR light. Only a handful of red supergiant spectra were available at the time. The synthetic spectra presented here represent an important step towards a more robust extension of previous work to ages between 5 Myr and a few 100 Myr.

2.1. New input spectra

The models in this paper use the empirical spectra of luminous red stars that were compared with theoretical spectra by Lançon et al. (2007a, hereafter LHLM07). They were acquired in part with CASPIR on the 2.3 m Telescope of the Australian National University (McGregor et al. 1994), in part with SpeX on NASA’s InfraRed Telescope Facility (Rayner et al. 2003). All the spectra cover wavelengths from 0.9 to 2.4 \( \mu \)m continuously, at \( \lambda/\delta \lambda \geq 750 \) (the SpeX data extend to 0.81 \( \mu \)m). The flux calibration through this wavelength range has been achieved using warm stars with known photometry. We refer to Lançon & Wood (2000) and Vacca et al. (2003) for the calibration methods applied respectively to the CASPIR and the SpeX data.

The theoretical spectra available to LHLM07 were computed with the PHOENIX code (P. Hauschildt and collaborators), for a metallicity typical of the sun but with surface abundances of C, N and O modified according to expectations from stellar evolution calculations. We refer to LHLM07 for a more complete description. The authors also describe and discuss the minimum-\( x^2 \) procedure used to estimate the effective temperature (\( T_{\text{eff}} \)), the surface gravity \( g \) and the extinction \( A_V \) of individual stars. The adopted extinction law is taken from Cardelli et al. (1989), with \( RV = 3.1 \).

The conclusions of LHLM07 most relevant to near-IR synthesis at \( R \sim 1000 \) are as follows: theoretical spectra are able to reproduce those of static red giants down to effective temperatures of about 3500 K; the models available to the authors did not as yet provide a satisfactory match of the spectra of cool and luminous red supergiants, even when the effects of internal mixing on surface abundances had been taken into account. Further theoretical work is being undertaken to improve the supergiant models; as yet, using theoretical spectra directly for population synthesis purposes is considered premature.

In order to build a suitable library for population synthesis purposes, the red supergiants and bright giants of the observed sample were subdivided into subsets of stars of class Ia, class Iab and class II/III. Each subset was sorted according to estimated \( T_{\text{eff}} \). Bins in \( T_{\text{eff}} \) were then constructed, containing between 1 and 5 stars depending on the number of spectra available in a given \( T_{\text{eff}} \) range, and depending on the individual quality of those data. The spectra in each bin were examined individually, and compared with spectra in neighbouring bins and in neighbouring luminosity classes. This had the purpose of removing or
reclassifying outliers, in order to obtain sequences along which spectral features evolve reasonably regularly. It must be kept in mind that, since synthetic spectra cannot reproduce the empirical spectra well, a large uncertainty affects estimated parameters such as $T_{\text{eff}}$ or $\log(g)$. Therefore, there is indeed quite some freedom for adjustment, especially for temperatures below 3800 K and for stars of class Ia and Iab.

The spectra within a given bin were then redetermined and averaged. All observed spectra cover wavelengths between 0.97 and 2.4 μm but only some extend to shorter wavelengths. Our bin averages all reach 0.51 μm: the best fitting model was used to extend the data in bins where no empirical short wavelengths spectra were available.

The resulting sequences have lower estimated values of $\log(g)$ for more luminous stars, as expected. The assigned values depend strongly on the assumed value of the microturbulence parameter in the stellar models. When using microturbulent velocities of only 2 or 3 km s$^{-1}$ (LHLM07), the stars of class Ia are assigned a value of $\log(g)$ of $-1$, i.e. a value that is not reached by standard sets of evolutionary tracks. With higher microturbulent velocity parameters (as suggested e.g. by studies of Tsuji et al. 1976; Gray et al. 2001; Origlia et al. 1993, 1997), $\log(g)$ rises to $-0.5$ or $0$ for the same class Ia spectra, and the spectral fits tend to improve (Lançon et al. 2007b). We have taken this trend into account qualitatively to locate the sequences in Fig. 1. At the time of this work, the grid of large microturbulence models has too coarse a sampling in $T_{\text{eff}}$ to allow us to also reassign temperatures consistently. This is an additional reason for uncertainty in the $T_{\text{eff}}$ values along the sequences of average spectra.

A procedure similar to the one just described has been applied (with much smaller uncertainties on the stellar parameters) to the empirical giant star spectra analysed by LHLM07. Together with the average spectra of long period variables and carbon stars of Lançon & Mouhcine (2002), this provides us with a library suitable for the construction of SSP spectra at both young and old ages. Details about the modelling of the older populations lie outside the scope of the present article.

2.2. Population synthesis assumptions and predictions

The synthesis of SSP spectra is performed with a version of the code PÉGASE,2 (Fioc & Rocca-Volmerange 1997, 1999) that has been adapted to our purposes following Mouhcine & Lançon (2002). The computation of isochrones from evolutionary tracks is unchanged, but red supergiant phases are flagged\(^2\). Non-flagged points along the isochrones are represented with spectra of the default library of PÉGASE,2, i.e. the semi-empirical library of Lejeune et al. (1998). Flagged points are represented with the new average spectra of red supergiants described above. The bolometric corrections needed to scale the fluxes are computed by forcing the near-IR spectra to match the level of the Lejeune spectra in the $J$ band. Other options for the bolometric corrections have not yet been explored. For the linear interpolation between the spectra of the three red supergiant sequences, we choose to proceed as follows: first we interpolate along each of the two bracketing sequences to reach the target $T_{\text{eff}}$, then we interpolate between the two resulting spectra according to $\log(g)$.

The stellar evolution tracks used in this paper are taken from Bressan et al. (1993). Our study is limited to near-solar metallicity (tracks at $Z = 0.02$) and we use the IMF of Salpeter (1955) unless otherwise stated. Any star initially more massive than 7 $M_\odot$ is flagged as a supergiant when it evolves off the main sequence. As a consequence, the new collection of supergiant spectra modifies the predictions of PÉGASE up to an age of about 75 Myr.

Figure 2 indicates which of the average red supergiant spectra contribute most strongly to the bolometric light of single-age populations at any given ages. Spectra of the class Ia sequence are dominant (among red supergiants) only at the youngest ages (7–8 Myr). Their contribution becomes negligible after about 15 Myr, but we note that this number is particularly sensitive to the value of the gravity assigned to the stars observed. Stars

\(^{1}\) Cf. http://www2.iap.fr/pegase/  
\(^{2}\) Red giant and asymptotic red giant phases are also flagged but this is relevant only to intermediate age and old populations.
of class Iab are dominant between ages of about 10 and about 25 Myr. Afterwards, the strongest red supergiant contributions to \( L_{\text{bol}} \) come from stars of class Ib/II.

The red supergiants all together are responsible for 70–85% of the 2 \( \mu \)m flux and 45–75% of the 1 \( \mu \)m flux, on average, at ages between 9 Myr and 65 Myr (see Sect. 5.2). Stars hotter than 5000 K provide the rest of the emission. Because the library of Lejeune et al. (1998) has a low resolution in the near-IR, our models will lack the high resolution spectral features of the warmer stars, and this is a caveat in particular at short wavelengths. For the main molecular bands in the H and K windows, implications are limited. Stars warmer than 5000 K have very little CO absorption at 1.6 \( \mu \)m and their contributions at 2.3 \( \mu \)m remain small.

As can be seen in Fig. 3, the new spectra do not only improve the spectral resolution but they also modify the energy distribution. With the adopted bolometric corrections (forced match with the old models in the J band), the J, H and K magnitudes are not changed significantly, but the flux around 1 \( \mu \)m is strongly modified for ages between 10 and 25 Myr. The molecular bands of CN (e.g. 1.1 \( \mu \)m, 1.4 \( \mu \)m) were not present at an appropriate level in the theoretical models that entered the semi-empirical library of Lejeune et al. (1998).

### Table 1. Observations of star clusters in M 82.

| Target | Date (d/m/yr(UT)) | Usable time on target | PA |
|--------|-------------------|-----------------------|----|
| L & F  | 31/3/02           | 2 x 120 s             | 22°|
| 1a & 1c| 3/4/02            | 2 x 240 s             | 125°|
| z      | 3/4/02            | 3 x 240 s             | 125°|
| nucleus| 3/4/02            | 4 x 240 s             | 22°|

### Fig. 4. Bright near-IR star clusters in the inner disc of M 82. Shown in inverted greyscale are two merged HST/NICMOS3 narrow H band archive images (filter F164N; HST program 7218, P.I. R. Rieke). The clusters discussed in the present article are labelled following the nomenclature of McCrady et al., (2003) and McCrady & Graham (2007).

### 3. Observations and the M 82 cluster sample

#### 3.1. Observations

Near-IR spectra of the nucleus and of five star clusters in M 82 were acquired with the infrared spectrograph SpeX (Rayner et al. 2003) mounted on the NASA Infrared Telescope Facility (IRTF), as detailed in Table 1. The targets were selected to be among the brightest near-IR sources in M 82. They are identified in Fig. 4, following the nomenclature of McCrady & Graham (2007).

The short wavelength setting of the SpeX instrument covers wavelengths from 0.81 to 2.4 \( \mu \)m in a single observation, thus eliminating some of the uncertainties inherent in the relative flux calibration of independent observations in the Z, J, H and K windows. Since many of the spectral features of interest are broad molecular bands that extend across the “forbidden” regions of high telluric absorption (telluric H\(_2\)O around 1.15, 1.4 and 1.9 \( \mu \)m), this is a significant advantage of SpeX over many other current instruments.

Observing conditions were not photometric, and as a compromise between spectral resolution and the need to collect photons, we used a 0.8” × 15” slit, giving a resolving power of \( R = 750 \). A fraction of the red supergiant stars were observed during the same run, with the same instrumental setting.

The targets were observed with SpeX in a series of individual exposures of 120 s or 240 s. Sky exposures were obtained for each frame at 140” to the South-East of the target position, well outside the main body of the galaxy. Several A0 type stars with known photometry were observed for the relative flux calibration and for the correction of telluric absorption (Vacca et al. 2003). In the end, the observations of the A0V star HD 92738 provided the best telluric correction for all the targets in M 82. The data reduction was based on the instrument-specific software package, Spextools, version 3.1 (Cushing et al. 2004). This software offers the possibility of rescaling the spectral segments of various...
orders after they have been flux calibrated and before they are merged. But, as expected when the calibration is successful, we found no need to apply such an order-dependent scaling factor.

The final merged spectra are shown in Fig. 5. They are available from the authors upon request.

### 3.2. The M 82 cluster sample

We now describe previous optical studies of our cluster sample; a summary of their derived ages and masses is given in Table 2.

Clusters M 82-F and M 82-L are located in the western disc outside the main star forming region. They have been studied previously using optical spectra that extended to about 9000 Å, and high resolution images (Gallagher & Smith 1999; Smith & Gallagher 2001; McCrady et al. 2005; Smith et al. 2006; Bastian et al. 2007). Cluster F is intrinsically fainter than L but is seen through a lower optical depth of dust; it appears brighter than L in the V band but fainter in K. Based on optical spectra the age favoured for cluster F lies between 40 and 80 Myr (Gallagher & Smith 1999; Smith & Gallagher 2001; Bastian et al. 2007). Dynamical mass estimates range from 4.7 \( \times 10^5 \) to 18 \( \times 10^5 \) \( M_\odot \) depending on the adopted stellar initial mass function (Smith et al. 2006). Dynamical masses have values of 7.6–9.6 \( \times 10^5 \) \( M_\odot \) for cluster 1a and 4.4–6.0 \( \times 10^5 \) \( M_\odot \) for cluster 1c (McCrady et al. 2007).

Cluster M 82-z is located in the eastern disc region known as region B (O’Connell & Mangano 1978). It is not mentioned in the optically selected cluster list for this region by de Grijs et al. (2001), and is also absent in the \( U \)-band selected cluster sample studied by Smith et al. (2007). Indeed, cluster z is barely detected at F555W in the HST/ACS Wide Field Channel mosaic of M 82 (Mutchler et al. 2007).

The high near-IR brightness of cluster z suggests that the cluster may be in the red supergiant-dominated phase of evolution, i.e. that it might be one of the youngest clusters in region B. Smith et al. (2007) find that the peak epoch of cluster formation in this region was ~150 Myr ago, with clusters forming at a lower rate until 12–20 Myr ago. To estimate the dynamical mass of cluster z, we combined the velocity dispersion measurement of McCrady et al. (2007) with a new radius measurement on the F814W image from the ACS mosaic of M 82 (Mutchler et al. 2007; measurement by I. Konstantopoulos, private communication). We found a mass range of 4.7–9.5 \( \times 10^5 \) \( M_\odot \).

### 4. Near-IR analysis

#### 4.1. Fitting procedure

The relative quality of the model fits to the near-IR spectrum of a given cluster is measured with a reduced \( \chi^2 \):

\[
\chi^2 = \frac{1}{N} \sum_i \left( \frac{S_i - \alpha M_i}{\sigma_i^2} \right)^2
\]

where \( i \) runs through the spectral pixels, \( S \) is the empirical spectrum, \( M \) the model under study, \( \alpha \) the factor that minimises \( \chi^2 \) for this model, and \( \sigma \) the estimated noise. \( W = 0 \) is used to mask regions where strong telluric absorption leaves strong residuals after correction. \( W \) also allows us to perform fits on selected, restricted wavelength ranges. \( N \) is the number of pixels with \( W = 1 \). The value of \( \chi^2 \) is useful only to compare the quality of various model fits to a given spectrum. Note that it does not fulfill the mathematical requirements (such as statistical independence of the data points) that would allow us to interpret its numerical values in terms of likelihoods.

The models considered are SSPs with ages between 1 and about 100 Myr, reddened using the family of extinction laws of Cardelli et al. (1989). The shape of these laws at near-IR wavelengths (\( >0.9 \mu m \)) is independent of the adopted value of \( RV = A_V/E(B-V) \). Therefore, the estimated near-IR age is independent of \( RV \). Constraints on \( RV \) are obtained when optical data are added to the near-IR spectrum. The estimated intrinsic (dereddened) luminosity of the cluster will be affected by the assumptions on the extinction law much more than the cluster ages.
weight the extinction law. Wavelengths outside the rectangular boxes have zero weight the \( \chi^2 \) minimisation procedure. The noise spectrum used to weight the \( \chi^2 \) is shown in light grey (cyan in the electronic version).

The \( \chi^2 \)-map of Fig. 9 shows a valley that illustrates the age-extinction degeneracy between age and extinction present in the colours alone indicate ages of 30–40 Myr. A restriction to wavelengths below 1.35 \( \mu \text{m} \) favours slightly younger ages, at which SSP models display deeper CN features, and a correspondingly lower extinction (we recall that the adopted extinction law. The figure shows that the age ranges found in these tests overlap nicely, globally favouring ages between 10 and 35 Myr. Note that the lower signal-to-noise ratio below 1.35 \( \mu \text{m} \) leads to a very shallow \( \chi^2 \) minimum in the corresponding curve. One final test was performed using the full wavelength range available, but allowing the extinction law to be modified by multiplication with a second order polynomial. Acceptable changes in the energy distribution were found to be limited to less than \( \sim 5\% \), and the resulting age range was not significantly affected. The value of \( R_V \) providing the best match to the global energy distribution correlates with age: \( R_V \approx 3.1 \) is found for ages near 10 Myr, \( R_V < 3.1 \) for older ages.

For the sake of completeness, Fig. 10 shows the best fit obtained assuming an age of 60 Myr, i.e. the age suggested by recent studies of the spectrum at wavelengths shorter than 1 \( \mu \text{m} \); although the energy distribution can be matched decently (with \( R_V \approx 2.7 \)), the fits to the molecular bands are poor. Within the framework of the set of SSP models described above (i.e. the new library of red supergiant spectra, the current estimate of the parameters of the library stars and the adopted set of stellar evolution tracks), an age of 60 Myr is excluded. We refer to Sect. 5 for a further discussion of model-dependence.

4.3. Cluster F

For cluster F, the best fit to the near-IR spectrum as a whole is obtained for ages around 35 Myr. The best model provides an excellent representation of the spectral features longwards of 1.06 \( \mu \text{m} \), and a good representation of the CN bands at shorter wavelengths (Fig. 11). This is confirmed by fits to individual near-IR wavelength windows (Fig. 12). The \( H \) and \( K \) band spectra alone indicate ages of 30–40 Myr. A restriction to wavelengths below 1.35 \( \mu \text{m} \) favours slightly younger ages, at which SSP models display deeper CN features, and a correspondingly lower extinction (we recall that \( R_V \) affects the value of \( A_V \) but not the quality of the fit at wavelengths \( > 0.9 \mu \text{m} \)). The bottom panel of Fig. 11 illustrates how well this younger model still reproduces the global energy distribution of cluster F. The age-extinction degeneracy is almost perfect: near-IR broad band colours alone could not have provided significant constraints on

Fig. 6. Best fit to the near-IR spectrum of cluster M 82-L (arbitrary units of energy per unit wavelength). The model (grey; red in the electronic version) follows the SpeX data (black) very closely over the whole range of that data (0.81–2.4 \( \mu \text{m} \)). It also matches the optical observations of Smith & Gallagher (2001; dotted) if one adopts \( R_V \approx 2.4 \) for the extinction law. Wavelengths outside the rectangular boxes have zero weight in the \( \chi^2 \)-minimisation procedure. The noise spectrum used to weight the \( \chi^2 \) is shown in light grey (cyan in the electronic version).

Fig. 7. Zoom on the \( H \) band of the fit of Fig. 6 (no additional renormalisation was required). The fit allows for a good measurement of the [FeII] emission line.

Fig. 8. Zoom on the \( K \) band of the fit of Fig. 6 (no additional renormalisation was required).
either the age or the amount of reddening within the age range of interest.

Cluster F has fainter magnitudes than cluster L in the near-IR and our SpeX data, taken simultaneously with cluster L through the same slit, have a lower signal-to-noise ratio. As a consequence, the χ²-curves for cluster F have lower contrast and a broader minimum than those for cluster L. Based on the current data and SSP models, we derive a conservative age range of 15 to 50 Myr for cluster F. The CO bands around 1.6 μm and CN bands of the 60 Myr model are uncomfortably weak compared to the observations. The near-IR age range overlaps with the younger of the optical ages from previous studies (Table 2).

In Fig. 13, optical spectra obtained with WHT/ISIS (Smith & Gallagher 2001) and HST/STIS (Smith et al. 2006) are shown. The model displayed corresponds to the best fit to the SpeX spectrum (34 Myr). R_V = 3.3 is chosen for a best match to the slope of the STIS spectrum. The STIS spectrum can be matched reasonably well together with the SpeX spectrum. In agreement with results from the SpeX data restricted to short wavelengths, a direct fit to the STIS spectrum alone favours the younger of the ages in the range already indicated. If future improvements of the model inputs lead to stronger near-IR molecular bands at older ages, a more satisfactory match between optical and near-IR ages might be obtained (see Sect. 5.1).

No combination of A_V and R_V provides a satisfactory fit to the more extended combined energy distribution of the SpeX and ISIS data. Efforts to improve the models should be accompanied with new observations of cluster F. Indeed, the direct comparison of the HST/STIS and WHT/ISIS spectra shows differences in the energy distribution, in the absorption features and in the strength of the nebular emission lines (Fig. 13). Considering the wealth of small scale structure around cluster F (McCrady et al. 2005; Bastian et al. 2007), it is not surprising that optical spectra one taken with HST/STIS, the other from the ground, differ. The near-IR SpeX spectrum, taken under poor seeing conditions through a relatively broad slit, covers a different area again. The ground based data could be contaminated by emission from younger stars on a neighbouring line of sight, which would also explain the presence of weak emission lines. The complex dust configuration could produce an obscuration law that differs from the ones we have explored here.

4.4. Luminous masses of clusters L and F

Based on the above results, we may estimate the luminous masses of clusters L and F and compare them with dynamical mass estimates. We adopt the cluster magnitudes of McCrady & Graham (2007), and assume a distance to M 82 of 3.6 Mpc.
We correct these magnitudes for extinction with the simplifying assumption that our measurement of the reddening indeed translates into extinction as in the dust screen model of Cardelli et al. (1998). In Fig. 14, the measured F160W magnitudes (which depend on age through the age-dependent estimate of extinction) are compared to predictions for single stellar populations with total stellar masses equal to the dynamical masses of Table 2. Our results for cluster F are consistent with previous work: the cluster indeed seems overluminous. At the favoured age of 34 Myr, it is a factor of 2 more luminous than the prediction based on a Salpeter IMF and on a mass of $1.3 \times 10^6 M_\odot$. For cluster L, the luminous and dynamical masses agree.

4.5. Clusters 1a and 1c

Because of poor seeing at the time of the observations, the spectra of clusters 1a and 1c are severely blended and only a combined spectrum has been extracted finally. It displays all the strong molecular bands typical of luminous red supergiants. Figure 15 shows the spatial profiles measured along the slit in two spectral orders, around 1.05 \( \mu m \) and around 2.15 \( \mu m \). The relative contributions of clusters 1a and 1c are similar at all extracted wavelengths, suggesting either similar ages for both clusters or a fortuitous compensation of an age difference with a difference in extinction. Therefore, we explore single-age population models before considering more complex combinations.

When fitting the spectrum with synthetic spectra of single-age populations (Fig. 16), the residuals show that the global curvature of the observed near-IR energy distributions are not matched quite as well as in the case of cluster L or cluster F. The best fitting models are peaked in the \( H \) band more than the data. The residuals are of the order of 10% only. Considering the high extinction towards the observed sources (\( A_V \approx 5 \)), we cannot exclude that such a difference may be due to an inadequacy of the adopted extinction law. An excellent fit is obtained when the extinction curve is modified with an ad hoc second order polynomial (which takes values between 1 and 1.1).

Figure 17 shows how the reduced \( \chi^2 \) varies with model age, depending on the wavelength range used to constrain the fit. The spectrum favours ages between 9 and 30 Myr, i.e. the ages at which the red supergiant features in the model spectra are strongest. The thick grey curve (green in the colour version of the figure) is obtained with the modified extinction law: the value of the best \( \chi^2 \) is reduced but the behaviour with age is otherwise unchanged.
Fig. 14. Absolute dereddened magnitudes of clusters L (top) and F (bottom). The asterisk shows the values favoured based on the near-IR analysis; dotted and dashed lines show the range of acceptable values. The solid lines are predictions, for masses that bracket the range of dynamical masses given in Table 2. A Salpeter IMF (0.1–120 $M_\odot$) is assumed.

Fig. 15. Spatial profiles across clusters 1a and 1c along the slit of the SpeX spectrograph (after background subtraction). The extracted aperture is indicated.

The analysis of the HST/STIS spectrum of cluster 1a by Smith et al. (2006) led to an age of 6 to 7 Myr with $E(B-V) = 1.35$ and $R_V = 3.1$ (we will refer to these estimates as the STIS-parameters below). An age this young is excluded in the framework of our near-IR analysis (Fig. 18): at ages younger than 9 Myr, the stellar evolution tracks of Bressan et al. (1993) do not allow cool supergiants to contribute enough to explain the deep molecular bands we see.

Could two-component models offer a satisfactory solution to this discrepancy? In other words, could a model for cluster 1a based on the STIS-parameters be combined with an older model for cluster 1c in such a way as to match the SpeX data? Within our current setting, the answer is no. The difference in colour between the model shown in Fig. 18 and the SpeX spectrum is incompatible with the small wavelength dependence of the spatial profile across the two clusters along the SpeX slit. The profile also excludes a solution in which an older, highly reddened cluster 1c would outweigh a bluer contribution from cluster 1a by large factors.

Our interpretation of the above discrepancy between optical and near-IR ages is that it is due to an inadequacy of the adopted set of stellar evolution tracks. Despite the impressive mismatch in Fig. 18, the difference between derived optical and near-IR ages is actually small. Between ages of 5 Myr and 10 Myr, the evolution in the ratio between red and blue stars is extremely
rapid, and therefore also particularly model dependent. Figure 2 of Fioc & Rocca-Volmerange (1997) shows that the predicted rapid transition from blue to red (V - K) colour occurs about 3 Myr earlier with the tracks of Meynet et al. (1994), used by Smith et al. (2006), than with those of Bressan et al. (1993), used here. Tracks that include stellar rotation, or tracks with slightly different metallicities, also modify the time at which first red supergiants appear by a few Myr.

4.6. Cluster z

Because of the extreme extinction towards cluster z, we were able to extract its SpeX spectrum only for λ > 1.13 μm. Figures 19 and 20 show the best fit obtained and the corresponding χ² curve. The near-IR constraints on age are similar to those obtained for cluster L and 1a: the molecular bands are strong and this selects ages at which the contributions of luminous red supergiants are important. Ages between 10 and 30 Myr are favoured. A closer look at the fits to the CO bands in the H and K window shows that even these young models produce CO bands that are marginally too weak compared to the data. Ages older than 40 Myr are excluded in the framework of our current models. Clearly, cluster z belongs to the very youngest objects in region B of M 82.

It is worth noting that the energy distribution through the near-IR range is extremely well reproduced with the extinction law of Cardelli et al. (1989), despite the high optical depth (AV ≃ 9.4 if RV = 3.1).

5. Discussion

5.1. Near-IR modelling

We have shown that it is possible to obtain very good representations of the near-IR spectra of young massive star clusters. The near-IR ages summarised in Table 2, however, do not always agree with previous optical ages. For the M 82 clusters under study, a general trend seems to apply: the near-IR spectra display deep molecular bands, and as a result they point to model ages at which the contributions of luminous red supergiants is important.

The input that most strongly affects the red supergiant contributions at any given age is the adopted set of evolutionary tracks. At ages between 5 and 100 Myr, large differences between the predictions for various available sets are obvious in colour plots, colour-magnitude diagrams and optical spectra (Fioc & Rocca-Volmerange 1997; Bruzual & Charlot 2003; Levesque et al. 2005; González Delgado et al. 2005). The tracks of the Geneva group (Schaller et al. 1992; Meynet et al. 1994; non-rotating tracks of Meynet & Maeder 2003) produce more and cooler red supergiants at young ages (6−20 Myr) than those of the Padova group, used here. Near-IR models based on the Geneva tracks may well be able reconcile the optical and near-IR ages of cluster M 82-1a. Stronger red supergiant contributions are also obtained at a variety of ages with tracks that assume newborn stars rotate (Meynet & Maeder 2000, 2003; Vázquez et al. 2007). Along rotating tracks, the stars tend to spend more time in redder parts of the HR-diagram, the red supergiants evolve at higher luminosities and lower (average) surface gravities, and they have strongly enhanced surface abundances of nitrogen. Both optical and near-IR studies would be affected by these changes.
The second model input of importance for stellar population synthesis is the spectral library. In Sect. 2.1, we noted that until the stellar atmosphere models are able to properly reproduce the extended spectra of individual red supergiants, the values of $T_{\text{eff}}$ and $\log(g)$ assigned to individual stars will remain uncertain. They are affected by metallicity, detailed surface abundances, microturbulence and other model atmosphere ingredients. As an illustration of the sensitivity of age dating techniques to these inputs we have computed SSP models in which the spectral sequences of Fig. 1 were shifted up (case A) or down (case B) in $g$ (by 0.4 dex for class Ia, 0.2 dex for class Iab). When assigned gravities are larger (case B; expected if microturbulent velocities are large), spectra of the more luminous sequences are used with larger weights and over a larger range of ages than when assigned gravities are small (case A). The strongest effect is a prediction of stronger CN bands with larger assigned gravities.

We confronted the resulting SSP spectra with observations of cluster F, for which the bluer parts of the near-IR spectrum (predominantly shaped by CN bands) indicated slightly younger ages than the $H$ and $K$ band spectra (Fig. 12). This situation suggested that models with stronger CN bands would provide a better global fit. As expected, case B models led to a wavelength independent near-IR age of 25−30 Myr, while case A made it impossible to match CN and CO bands simultaneously.

This test shows that with the data quality achievable today we are sensitive to spectral differences between luminosity subclasses, and it will be useful to continue to include this distinction in future population synthesis models.

The derived ages are expected to be sensitive also to the adopted $T_{\text{eff}}$ scale. Assigned temperatures rise by up to 300 K when the microturbulence parameter is increased to 10 km s$^{-1}$, but (based on a very preliminary exploration of a new series of theoretical spectra) they drop by similar amounts when switching from the solar abundances of Anders & Grevesse, used here (see LHL07), to those of Asplund et al. (2005).

In view of the above, it is clear that it will be necessary to reassess the cluster data with a wider range of models. The large systematic errors due to the choice of a particular model, which are not included in Table 2, can then be quantified and reduced by selecting the subset of models providing satisfactory simultaneous fits to both the optical and the near-IR data.

5.2. Stochastic fluctuations

The issue of stochastic fluctuations is the result of the contrast between the small fractional number of bright stars in a stellar population and their large contribution to the luminosity (Girardi & Bica 1993; Santos & Frogel 1997; Lançon & Mouhcine 2000; Cerviño & Luridiana 2006). Table 3 lists the average relative and absolute numbers of red supergiant stars in synthetic single-age populations of total mass $10^6 M_\odot$ as well as the contribution of these stars to the flux at 1 $\mu$m and 2.2 $\mu$m. Note that these numbers depend on the shape of the IMF. Poisson statistics tell us that the rms dispersion in the actual number of red supergiants between single clusters of that mass equals the square root of the average number. In the $K$ band, the red supergiants are so much more numerous than other coeval stars that these variations translate almost directly into dispersions in the fluxes (Lançon & Mouhcine 2000). For colours such as $V-K$ or $Z-K$, fluctuations are also due partly to varying numbers of luminous blue stars. When average numbers are small ($<10$), the predictions can be offset from the mean or multimodal: the colours vary wildly depending on whether or not a handful of massive stars happen to be in a red or in a blue phase of their evolution.

Table 3 tells us it is necessary to work with clusters of $\sim 10^6 M_\odot$ or more, if one wishes to test detailed model ingredients (unless large samples of clusters are available for a statistical analysis). For instance, at an age of 30 Myr a cluster of $\sim 10^6 M_\odot$ will contain 260 ± 16 red supergiants, that will on average provide 85% of the $K$ band flux. Clearly, the ∼6% fluctuations in the red supergiant numbers (combined with fluctuations in the numbers of blue stars) will produce a spread in colours such as $V-K$ that make it impossible to test the small differences in average properties resulting from conservative changes in the IMF.

The differences between evolutionary tracks are much larger than those associated with changes in the IMF. We expect that at least some of these will be testable with individual clusters more massive than a few $10^5 M_\odot$. Detailed computations with the various sets of tracks now available will be needed in order to verify this statement. As a general rule, even with masses around $10^6 M_\odot$, the existence of the fundamental stochastic limitation must be kept in mind.

6. Conclusion

Using new synthetic spectra of single stellar populations that extend to 2.5 $\mu$m and include red supergiant spectra at resolution $\lambda/\Delta \lambda = 750$, we have analysed the near-IR spectra of a few of the most massive star clusters in the starburst galaxy M 82.

We demonstrate that very good fits to all the near-IR photospheric features seen at this resolution can now be obtained. In particular, the new synthetic spectra can be used for a precise subtraction of the stellar background in emission line

\begin{table}
\centering
\caption{Average numbers and flux contributions of red supergiant stars in single age populations containing $10^6 M_\odot$ of stars. Here any star with an initial mass above 7 $M_\odot$ and an effective temperature below 4900 K is counted as a red supergiant. The IMFs are from Salpeter (1955) and Kroupa (1993). The lower mass cut-off is 0.1 $M_\odot$ for the upper lines, 0.6 for lower lines.}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline
Age (Myr) & Absolute number (Salpeter) & Fractional number (Salpeter) & Fractional contribution at 1 $\mu$m (Salpeter) & Fractional contribution at 2.2 $\mu$m (Salpeter) & Absolute number (Kroupa) & Fractional number (Kroupa) & Fractional contribution at 1 $\mu$m (Kroupa) & Fractional contribution at 2.2 $\mu$m (Kroupa) & Fractional contribution at 2.2 $\mu$m (Kroupa) \\
\hline
8 & 60 & 2.0 $\times 10^{-3}$ & 28% & 44% & 40 & 1.8 $\times 10^{-3}$ & 27% & 43% & 43% \\
10 & 150 & 5.2 $\times 10^{-3}$ & 72% & 87% & 100 & 4.9 $\times 10^{-3}$ & 68% & 85% & 85% \\
30 & 260 & 8.3 $\times 10^{-3}$ & 64% & 86% & 220 & 1.0 $\times 10^{-2}$ & 59% & 84% & 84% \\
60 & 360 & 1.3 $\times 10^{-2}$ & 49% & 73% & 340 & 1.7 $\times 10^{-2}$ & 46% & 70% & 70% \\
8 & 120 & 2.4 $\times 10^{-2}$ & 28% & 44% & 60 & 9.1 $\times 10^{-3}$ & 27% & 43% & 43% \\
60 & 730 & 1.5 $\times 10^{-1}$ & 49% & 73% & 570 & 8.6 $\times 10^{-2}$ & 46% & 71% & 71% \\
\hline
\end{tabular}
\end{table}
studies. The models also significantly improve predictions of the low resolution energy distribution around 1 μm over those based on previous stellar libraries. Further improvements around 1 μm are to be expected from the inclusion of stars warmer than 5000 K in the library of near-IR spectra used here.

Between ages of 10 and 60 Myr, we have found that the degeneracy between age and extinction is essentially perfect in near-IR broad band photometry (Y, J, H, K), when the extinction law of Cardelli et al. (1989) is used. A simultaneous fit of the near-IR spectra and the optical + near-IR energy distribution was obtained for cluster M 82-L, and this required a modified extinction law (e.g. the law of Cardelli et al. 1989, with R_V < 3.1). This new evidence for non-standard extinction laws towards star clusters in starburst galaxies, which is not surprising considering the very inhomogeneous spatial distribution of the dust in these objects, is an additional difficulty in any attempt to derive ages from photometry alone. The use of extended spectra allows to constrain both the ages and the shape of the extinction law. It is worth recalling, however, that a given shape of the extinction law can correspond to a variety of values of the total amount of obscuration (e.g. Witt & Gordon 2000).

A table of red supergiant numbers and flux contributions has been provided. We argue that the stochastic nature of the stellar mass function must be kept in mind at all cluster masses, but that this new evidence for non-standard extinction laws towards star clusters in starburst galaxies, which is not surprising considering the very inhomogeneous spatial distribution of the dust in these objects, is an additional difficulty in any attempt to derive ages from photometry alone. The use of extended spectra allows to constrain both the ages and the shape of the extinction law. It is worth recalling, however, that a given shape of the extinction law can correspond to a variety of values of the total amount of obscuration (e.g. Witt & Gordon 2000).

The absolute ages derived from the near-IR spectra depend on model parameters that are still highly uncertain, to a large part because the physics of red supergiants (evolution, spectra) are particularly complex. More work on the stellar models and more confrontations with star cluster data will be needed. Care needs to be taken in matching the apertures of multi-wavelength observations. It is promising that data quality now allows us to exploit “details” that were neglected until now, such as the differences between spectra of supergiants of class Ia, Ib and II/III.

The near-IR ages found with the current model assumptions for the observed IR-bright clusters in M 82 are concentrated between 9 and 35 Myr. Indeed, their spectra display deep bands of CN and CO, and therefore favour the model ages at which the contributions of luminous red supergiants are strongest. Cluster F, with weaker bands, is the oldest cluster of our sample. In most cases, the near-IR molecular bands of the models at the ages derived from optical studies are marginally acceptable or too weak. Changing the adopted evolutionary tracks or the parameters assigned to the spectra of the input stellar library can result in deeper near-IR bands over a wider range of ages. Work is in progress to perform these tests, which should in time allow us to select the theoretical model inputs most appropriate for the analysis of star clusters in starburst galaxies.

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