Bacteriophages affect evolution of bacterial communities in spatially distributed habitats: a simulation study

Alexandra Igorevna Klimenko 1,2*, Yury Georgievich Matushkin 1, Nikolay Alexandrovich Kolchanov 1,2 and Sergey Alexandrovich Lashin 1,2

From The 7th International Young Scientists School “Systems Biology and Bioinformatics” (SBB’2015) Novosibirsk, Russia. 22-25 June 2015

Abstract

Background: Bacteriophages are known to be one of the driving forces of bacterial evolution. Besides promoting horizontal transfer of genes between cells, they may induce directional selection of cells (for instance, according to more or less resistance to phage infection). Switching between lysogenic and lytic pathways results in various types of (co)evolution in host-phage systems. Spatial (more generally, ecological) organization of the living environment is another factor affecting evolution. In this study, we have simulated and analyzed a series of computer models of microbial communities evolving in spatially distributed environments under the pressure of phage infection.

Results: We modeled evolving microbial communities living in spatially distributed flowing environments. Non-specific nutrient supplied in the only spatial direction, resulting in its non-uniform distribution in environment. We varied the time and the location of initial phage infestation of cells as well as switched chemotaxis on and off. Simulations were performed with the Haploid evolutionary constructor software (http://evol-constructor.bionet.nsc.ru/).

Conclusion: Simulations have shown that the spatial location of initial phage invasion may lead to different evolutionary scenarios. Phage infection decreases the speciation rate by more than one order as far as intensified selection blocks the origin of novel viable populations/species, which could carve out potential ecological niches. The dependence of speciation rate on the invasion node location varied on the time of invasion. Speciation rate was found to be lower when the phage invaded fully formed community of sedentary cells (at middle and late times) at the species-rich regions. This is especially noticeable in the case of late-time invasion.

Our simulation study has shown that phage infection affects evolution of microbial community slowing down speciation and stabilizing the system as a whole. This influencing varied in its efficiency depending on spatially-ecological factors as well as community state at the moment of phage invasion.

Keywords: Microbial community, Bacteria, Archaea, Bacteriophage, Phage, Ecological simulation, Evolution, Evolutionary modeling, Prokaryotes

Background

Bacteriophages are known to be one of the driving forces of bacterial evolution [1–3]. It is generally thought that phages are responsible for about 10–50 % of the total bacterial mortality in surface waters, and 50–100 % in environments that are unfriendly to protists, such as low-oxygen lake waters [4]. Besides promoting horizontal transfer of genes between cells [5–7], they may induce either directional selection of cells [8], for instance, according to more or less resistance to phage infection [9–12], or fluctuating selection [10, 13]. Switching between lysogenic and lytic pathways results in various types of (co)evolution in bacterial cell-phage systems [14, 15]. Spatial (more generally, ecological) organization of the living environment is another factor affecting evolution [16–18]. A number of studies, both experimental and theoretical have...
recently been published on various aspects of phage-bacteria evolution.

The population mixing increasing host exposure to phages via selection for greater resistance and infectivity ranges was proved to promote arms-race dynamics [13]. It explains the variation in coevolutionary dynamics between different host–parasite systems, and more specifically the observed discrepancies between laboratory and field bacteria–virus coevolutionary studies [13]. Using a spatially explicit, individual-based model, it was shown that less infective pathogens may have an advantage in spatially structured populations, even when well-mixed models predict that they will not [19].

In a time-shift experiment with both sympatric and allopatric phages from either contemporary or earlier points in the season, it was demonstrated that bacterial resistance is higher against phages from the past, regardless of spatial sympathy or how much earlier in the season phages were collected [20]. It was also shown that future bacterial hosts are more resistant to both sympatric and allopatric phages than contemporary bacterial hosts. Nutrients availability was both theoretically and experimentally shown to affect the relative extent of escalation of resistance and infectivity (arms race dynamic) and fluctuating selection (fluctuating selection dynamic) in experimentally coevolving populations of bacteria and viruses [21]. Scanlan and colleagues have shown that in addition to affecting genome-wide evolution in loci not obviously linked to parasite resistance, coevolution can also constrain the acquisition of mutations beneficial for growth in the abiotic environment [22]. The conditions for achieving coexistence on the edge between two habitats, one of which is a bacterial refuge with conditions hostile to phage whereas the other is phage friendly were theoretically studied in [23]. They analyzed how bacterial density-dependent, or quorum-sensing, mechanisms such as the formation of biofilm can produce such refuges and edges in a self-organized manner.

A multiscale model of dynamic coevolution between hosts and viruses in an ecological context incorporating CRISPR immunity principles was presented in [24]. Hosts and viruses were shown to coevolve to form highly diverse communities. They observed evolutionary dynamics consistent with both incomplete selective sweeps of novel strains (as single strains and coalitions) and the recurrence of previously rare strains. Coalitions of multiple dominant host strains were predicted to arise because host strains can express nearly identical immune phenotypes mediated by CRISPR defense albeit with different genotypes [24]. The evolution of generalism in well-mixed populations was found to be highly sensitive to the severity of associated fitness costs, but the constraining effect of costs on the evolution of generalism is lessened in spatially structured populations [25]. The contrasting outcomes between the two environments was explained by different scales of competition (i.e., global vs. local). They suggested that local interactions may have important effects on the evolution of generalism in host-parasite interactions, particularly in the presence of high fitness costs [25].

In our previous study [26] we modeled the opposite trends of genome amplification/simplification occurred in microbial communities via gene horizontal transfer/gene loss. It was demonstrated that species with reduced genomes tend to replace genetically and metabolically rich species under highly favorable environmental conditions. Under unfavorable conditions, the opposite tendency was observed. It was also shown that phages invasion into the system radically changed the current evolutionary trends.

A wide range of mathematical and computational techniques is used for modeling and simulation of phage-bacterium systems. There are both classical ODE/PDE approaches (see examples in [11, 27–31]) and modern agent-based and/or multiscale approaches (see examples in [19, 23, 25, 32, 33]).

In this study, we have built and simulated a series of computer models of microbial communities evolving in spatially distributed environments under the pressure of phage infection. Communities inhabited spatially distributed flowing environments. Non-specific nutrient supplied in the only spatial direction, resulting in its non-uniform distribution in environment. We varied the time and the location of initial phage invasion as well as switched chemotaxis on and off and observed that these factors may lead to different evolutionary scenarios.

**Methods**

**Model overview**

We have used the Haploid evolutionary constructor (HEC) [34, 35] to build the model and to perform the simulations. The HEC models microbial community consisting of different microbial species which we call populations. The hierarchical scheme of HEC models is shown in Fig. 1. Each population consists of cells sharing the same metabolic specificity i.e. nutrients consumed and products secreted. We assume that metabolic pathways of substrates utilization and products synthesis controlled by corresponding gene networks are the same for all cells of a population. Therefore, we consider genes just as numerical parameters of these gene network models. The parameters may be responsible for efficiency of either utilization or synthesis of metabolites. Note that the HEC architecture provides various mathematical formalisms to be used to describe a gene network model mathematically (see details in [35]). In this case, mutations just change the numerical value of a certain parameter in one or several cells (which is interpreted as an origin of novel allelic variant) resulting in genetic polymorphism in a population. On the other hand, selection of more fit allelic combinations leads to
the extinction of weaker alleles decreasing the polymorphism. Horizontal transfer of genes between cells of different populations is modeled in HEC via rearrangement of recipient cell’s gene network by embedding additional nodes into this network (Fig. 2). Loss of genes is modeled in the same manner, nodes, of course, are deleted. We suppose in our model, that such events of horizontal gene transfer and gene loss are associated with the origin of novel species as they significantly change the metabolic properties of cells. Technically, we use in HEC the super-individual concept [36, 37].

Spatially distributed habitats
We describe the spatial organization of environment by a grid of so-called point environments or nodes – small well-mixed volumes containing cells, phage particles and...
substances. These volumes exchange their contents affected by diffusion and flow as well as during the bacterial chemotaxis activity (Fig. 3, detailed description in [38]). Flow is a directed force mixing contents of the spatial system and drawing particles from its beginning to the end. On the contrary diffusion is considered as undirected dissemination of the point environment’s contents. Chemotaxis is an ability of bacterial cells to move towards the attractants and away from repellents, i.e. a capacity to move to a habitat with more chemically beneficial conditions. Such a grid of multiple well-mixed volumes is capable to simulate heterogeneous distributions of cells, substances and phage particles.

We considered 2D spatially distributed flowing habitat represented as a 5x5 grid (Fig. 3). In-flow supplies the habitat with non-specific nutrients we call non-specific substrates through the upper and leftmost nodes. The flow and diffusion then spread nutrients over all other nodes of the habitat including not only non-specific substrates, but also metabolites synthesized and secreted by cells (specific substrates). Cells themselves are also passively transported by the flow and diffusion, but additionally may move via chemotaxis (details in [38]). Thus, the (1,1) node and its neighbors may be considered as nutrient-rich (in terms of non-specific substrates), while the (5,5) node and its neighbors are nutrient-poor (in the same terms). Here and after let us call the (1,1) node as the “top”, the (3,3) – “middle”, and the (5,5) – “bottom” of the habitat. It should be noted that we have tested the 10 × 10 and 20 × 20 habitats and found no principal difference with the 5 × 5 case.

**Modeling bacteriophage infection**

In the HEC, bacteriophages (phages) are described using special type of populations – phage populations, which are capable to infect microbial cells. In this particular case the phage was able to infect those cells which are capable to utilize S1 substrate. The infection process includes the following stages:

1. infestation of healthy cells by phage invasion (from environment into some cells of a population);
2. phages reproduction inside the infected cells;
3. phage burst after cell lysis.

Infected cells may develop then according to either lytic or lysogenic pathway. In the first case, the infected cells die bursting new phages into the habitat. In the second case, on the contrary, no cell die, phage genes are integrated into cell genome and the cells become prophages. The choice of lysogenic or lytic scenarios depends on environmental conditions and cells well-being at the moment of infestation (it is in accordance with biologically known facts [39]). Under favorable conditions, in the case of a positive population dynamics ensured by high environmental substrate concentrations and/or better genetic adaptation compared to other populations, the infection process occurs along the lytic pathway. Otherwise, under
unfavorable conditions, infection takes the lysogenic pathway. Later, if the conditions are improved, a part of the population may switch to the lytic pathway, which is followed by the death of this part of the population and generation of phages. The detailed description of the modeling technique for phages in the HEC is presented in [26]. In this study, we considered invasion of phages varying both the moment of invasion and its localization.

**Results and discussion**

Using the approach described above, we have developed a model of spatially distributed microbial community under bacteriophage attack. We started simulations with the simple symbiotic community of three different populations (Fig. 4) uniformly inhabited spatially distributed 2D environment (Fig. 3).

In the course of evolution the processes of horizontal gene transfer and gene loss stochastically simulated. It was associated with the origin of novel species (see details in the previous chapter). Initial environmental conditions promoted the origin of species possessing more and more complex genomes built combinatorically from relatively simple genomes of initial cells, as it was previously studied in [40]. We varied the time of initial phage invasion as well as its localization. The main questions we wanted to discover were the following:

- how does the phage invasion affect the ecological-evolutionary trends taking course in the community?
- what is the role played by spatial factors in found effects?
- is the bacteriophage an impediment for microbial communities' evolution?

Varying the time of initial phage invasion, we have found that infestation in general inhibits speciation, and after a certain time the species composition and the size of the community become stationary (Fig. 5, Additional file: 1). It looks as if the phages stop the evolution of the community. It should be noted that we talk about speciation in terms of variation of gene set involved in metabolic networks and the evolution of immune mechanisms is out of scope in this simulation study. It explains why we observe decrease in a speciation rate under phage invasion conditions whereas other studies [2] putting an emphasis on the evolution of defense and

---

**Fig. 4** Trophic graph of the initial community. N1 – non-specific substrate consumed by all populations (P1, P2, P3) of the community. S1, S2, S3 – specific substrates synthesized by corresponding cells. P1S2 means that cells of P1 population produce S2 substrate, which is consumed by cells of P2 population.

**Fig. 5** SRI in the first 5000 generations in various nodes.
Table 1  Average SRI values before and after phage invasion in various habitat locations (see Additional file 4). First 1000 generations has not been taken into account as there is a bias associated with high initial speciation

| Node location | Early-time (1st generation) SRI | Middle-time (5000th generation) SRI | Late-time (6600th generation) SRI |
|---------------|---------------------------------|--------------------------------------|----------------------------------|
| Into node (1,1) | SRI before: -8.56e-3 | SRI after: 6.850e-3 | SRI before: -5.20e-3 | SRI after: 7.143e-3 |
| Into node (3,3) | SRI before: -7.44e-3 | SRI after: 7.275e-3 | SRI before: -4.00e-3 | SRI after: 7.946e-3 |
| Into node (5,5) | SRI before: -5.78e-3 | SRI after: 8.250e-3 | SRI before: -6.00e-3 | SRI after: 6.964e-3 |

Fig. 6  Average number of species (up) and biomass (down) over the first 5000 generations in various nodes (see also the script in Additional file 3)
counter-defense strategies provide evidences of increasing phage and bacterial evolution rate. The other possible reason of the discrepancy is because we focused primarily on interactions between bacteria and temperate phages, rather than lytic phages as it has been done in the above-mentioned case.

We obtained the same results when chemotaxis was switched on/off. This effect has been estimated using the Speciation Rate Index (SRI), which was calculated according to the following formula (see also script file in Additional files):

$$SRI = \frac{\| \{ p | p \text{-newly emerged viable populations} \} \|}{\text{time span}}$$

(1)

where time_span is the period speciation rate is estimated about; a population is assumed to be viable if it survived over a period of three generations (where thres is a threshold value, in our case, 500). According to the equation 1, the higher SRI is, the more intensive the speciation is over this time period. Conversely, the lower SRI is, the fewer viable species originate in time.

**Chemotaxis-off case**
Initially, we have estimated SRI in all spatial nodes of the habitat in the absence of phage invasion (Fig. 5). Fig. 5 shows that speciation rate growth according to moving away from the in-flow (top) nodes. It could be explained by the fact that in top nodes there are several populations, which effectively utilize the non-specific substrate. These population have got dominate biomass. At the same time, novel ecological licenses associated with high concentrations of specific substrates arise in middle and top nodes due to transportation via the flow. It opens possibilities for fixation of novel species specialized on utilization of those specific substrates. That is to say, in distant, bottom nodes, higher biodiversity is associated with low biomass (Fig. 6).

After that, we have analyzed how the phage invasion affects speciation rate and species richness. Results obtained show the dependency of speciation rate on invasion parameters (Table 1).

Table 1 shows that phage invasion results in decrease of speciation rate by more than one order. As is easy to see the time dependency of speciation rate varies with the distance between the node and in-flow location:

1. In the case of early-time invasion, there is an inverse dependence – the farther the place of invasion, the less the speciation rate after infestation (Fig. 7).
2. In the case of middle-time invasion, the lowest speciation rate is observed when the phage invades the

![Average SRI after phage invasion](image-url)
central node (3,3) of the habitat. It is notable that if the phage invades the most bottom node (5,5), then average SRI becomes higher compared to the most top node (1,1).

3. In the case of late-time invasion, results look similar to the previous case except that average SRI is lower when the phage invaded central and bottom nodes.

As it was previously said, distant nodes are characterized by higher concentrations of the specific substrates. Therefore, these results are in accordance with earlier reported [41] suggestion that the viral effect is probably larger in eutrophic waters than in oligotrophic waters.

Table 2 shows that in the case of middle-time invasion, average SRI increases from top (1,1) nodes (non-specific

Fig. 8 Distributions of average values for (a) species richness; (b) SRI; (c) total biomass in spatial nodes. Values were calculated for the first 5000 generations.
substrate-rich) to bottom (5,5) nodes (non-specific substrate-poor). Additional plots (see Additional file: 2) show that the phage invasion leads to drastic reduction of species richness of the community. The data confirm that SRI as well as species richness are higher in the absence of phages and when there are many ecological licenses.

Chemotaxis-on case
In cases when chemotaxis is switched on (see Additional file 5), the spatial stratification of a community in terms of biomass is more expressed. We hypothesize that this is due to the observed accumulation of specific substrates in nodes close to the bottom of the habitat. Anyway, the distributions of species richness and SRI in general look similarly to the corresponding distributions obtained for the previous case. However, the spatial differences here are more evident (Fig. 8). On the other hand, the total species number as well as SRI in this case (chemotaxis is on) are definitely lower compared to the previous case (chemotaxis is off). It is in good agreement with evolutionary biology data postulating that migration impedes speciation while isolation promotes it [42–44].

Figure 9 shows that phage invasion into the bottom node (5,5) led to the growth of speciation rate both for early-time and late-time cases. It is related to the observed fact that the phage infection could not fixate in the habitat when invaded into bottom nodes. However, in the chemotaxis-on case, if the phage invaded top nodes, the species richness observed to be higher in bottom nodes.

Conclusions
In this simulation study, we have shown that bacteriophages may act as constraining factors of microbial community evolution. Phage infection decreases the speciation rate by more than one order as far as intensified selection blocks the origin of novel viable populations/species, which could carve out potential ecological niches. At the same time, phages act as a stabilizing factor suspending superfluous speciation and encouraging stationary state of the system (in terms of species number).

It has also been shown that the dependence of speciation rate on the invasion node location varied on the time of invasion. Speciation rate is found to be lower when the phage invaded fully formed community (middle and late times) at the species-rich nodes (central node (3,3)). This is especially noticeable in the case of late-time invasion.

Those dependencies differ in the case of chemotaxis switched on. In both early-time and late-time cases, the speciation rate remains relatively high when phage invaded bottom nodes. This phenomenon requires additional investigations.

As a result, our simulation study shows that phage infection affects evolution of microbial community slowing down speciation and stabilizing the system as a whole. This influence varied in its efficiency depending
on spatially-ecological factors as well as community state at the moment of phage invasion.

Additional files

Additional file 1: Data processing script addZeros.sce. A Scilab script.

Additional file 2: Data processing script speciation_rate.sce. A Scilab script.

Additional file 3: Data processing script averageSRandBiomass.sce. A Scilab script.

Additional file 4: SRLSR.Biomass.chemonoff.xlsx. An Excel spreadsheet.

Additional file 5: SRLSR.Biomass.chemon.xlsx. An Excel spreadsheet.

Additional file 6: Phage.extinction.chemon.xlsx. An Excel spreadsheet.

Abbreviations

HEC: Haploid evolutionary constructor software; SRI: Speciation rate index.

Competing interests

The authors declare that they have no competing interests.

Authors’ contributions

KAI and LSA have developed and simulated the models. KAI, MYUG, KNA and BN have contributed to biological discussions and help in interpretation of simulation results. KAI and LSA have written the paper. All authors have read and approved the final manuscript.

Acknowledgements

We would also like to thank Valentin Suslov (ICG SB RAS, Novosibirsk) for biological discussions and help in interpretation of simulation results.

Declarations

The study has been partially funded by the RFBR grant 150703879 (software implementation of 3D HEC modules) Budget Project 0324–2015–0003 (software implementation of other HEC modules) and the RSF grant N 142400123 (construction and computational analysis of evolutionary models). This article has been published as part of BMC Microbiology Volume 16 Supplement 1, 2016. Selected articles from the 7th International Young Scientists School “Systems Biology and Bioinformatics” (SBB 2015): Microbiology. The full contents of the supplement are available online at http://www.biomedcentral.com/bmcmicrobiol/supplements/16/S1.

Published: 27 January 2016

References

1. Hendrix RW. Bacteriophage Evolution and the Role of Phages in Host Evolution. In: Waldor MK, et al. Phages: their role in bacterial pathogenesis and biotechnology. American Society of Microbiology; 2005:55–65.
2. Koskella B, Brockhurst MA. Bacteria–phage coevolution as a driver of ecological and evolutionary processes in microbial communities. FEMS Microbiol Rev. 2014;38:916–31.
3. Prid E, Wassenaar T, Ghoose C, Blaser M. Evidence of host-virus co-evolution in tetrads nucleotide usage patterns of bacteriophages and eukaryotic viruses. BMC Genomics. 2006;7B.
4. Fuhrman JA. Marine viruses and their biogeochemical and ecological effects. Nature. 1999;399:541–8.
5. Ochman H, Lawrence JG, Groisman EA. Lateral gene transfer and the nature of bacterial innovation. Nature. 2000;405:299–304.
6. Canchaya C, Fournous G, Chibani-Chennoufi S, Dillmann M-L, Brüssow H. Phage as agents of lateral gene transfer. Curr Opin Microbiol. 2003;6:417–24.
7. Skippington E, Ragan MA. Lateral genetic transfer and the construction of genetic exchange communities. FEMS Microbiol Rev. 2011;35:707–35.
8. Bohannan BJM, Lenski RE. Linking genetic change to community evolution: insights from studies of bacteria and bacteriophage. Ecol Lett. 2000;3:362–77.
9. Desiere F, McShan WM, van Sinderen D, Ferretti JJ, Brüssow H. Comparative genomics reveals close genetic relationships between phages from dairy bacteria and pathogenic streptococci: evolutionary implications for prophage-host interactions. Virology. 2001;288:325–41.
10. Williams HT. Phage-induced diversification improves host evolvability. BMC Evol Biol. 2013;13:17.
11. Bemrgruber TW, Froissart R, Choisy M, Gandon S. Evolution of virulence in emerging epidemics. PLoS Pathog. 2013;9:e1003209.
12. Roberts PD, Portfors CV. Design principles of sensory processing in cerebellum-like structures. Early stage processing of electrosensory and auditory objects. Biol Cybern. 2008;98:491–507.
13. Gomez P, Ashby B, Buckling A. Population mixing promotes arms race host-parasite coevolution. Proc R Soc B Biol Sci. 2014;282:104297–9.
14. Heilmann S, Snepken K, Krishna S. Sustainability of virulence in a phage-bacterial ecosystem. J Virol. 2010;84:3016–22.
15. Levin BR, Moineau S, Bushman M, Barrangou R. The population and evolutionary dynamics of phage and bacteria with CRISPR-mediated immunity. PLoS Genet. 2015;11:e1003312.
16. Perfetto L, Pereira MI, Campos PRA, Gordo I. The effect of spatial structure on adaptation in Escherichia coli. Biol Lett. 2008;4:57–9.
17. Mitri S, Xavier JB, Foster KR. Social evolution in multispecies biofilms. Proc Natl Acad Sci U S A. 2011;108(Suppl):10839–46.
18. Lion S, Gandon S. Evolution of spatially structured host-parasite interactions. J Evol Biol. 2015;28:10–28.
19. Roychoudhury P, Shekhar N, Wiss VR, Krone SM. Fitness benefits of low infectivity in a spatially structured population of bacteriophages. Proc R Soc B Biol Sci. 2013;281:20132563–3.
20. Koskella B, Parr N. The evolution of bacterial resistance against bacteriophages in the horse chestnut phyllophore is general across both space and time. Philos Trans R Soc B Biol Sci. 2015;370:20140297.
21. Lopez Pascua L, Hall AR, Best A, Morgan AD, Boots M, Buckling A. Higher resources decrease fluctuating selection during host-parasite coevolution. Ecol Lett. 2014;17:1380–8.
22. Scanlan PD, Hall AR, Blackshields G, Friman V-P, Davis MR, Goldberg JB, et al. Coevolution with bacteriophages drives genome-wide host evolution and constrains the acquisition of abiotic-beneficial mutations. Mol Biol Evol. 2015;32:1425–35.
23. Helmann S, Snepken K, Krishna S. Coexistence of phage and bacteria on the boundary of self-organized refuges. Proc Natl Acad Sci U S A. 2012;109:12828–33.
24. Childs UM, Feld NL, Young MJ, Whittaker RJ, Weitz JS. Multiscale model of crispr-induced coevolutionary dynamics: diversification at the interface of lamarck and darwin. Evolution (N Y). 2012;66:2015–29.
25. Ashby B, Gupta S, Buckling A. Spatial structure mitigates fitness costs in host-parasite coevolution. Am Nat. 2014;183:E64–74.
26. Lashin SA, Matushkin YG, Suslov VV, Kolchanov NA. Evolutionary trends in the prokaryotic community and prokaryotic community-phage systems. Russ J Genet. 2011;47:1487–95.
27. Lenski RE, Levin BR. Constraints on the coevolution of bacteria and virulent phage: a model, some experiments, and predictions for natural communities. Am Nat. 1985;125:582–602.
28. Wang J-N, Dykhuisen DE, Stobodkin LB. The evolution of phage lysis timing. Evol Ecol. 1996;10:545–58.
29. Nowak MA, May RM. Superinfection and the evolution of parasite virulence. Proc R Soc B Biol Sci. 1994;255:81–9.
30. Abendon ST, Culler RR. Bacteriophage evolution given spatial constraint. J Theor Biol. 2007;248:111–9.
31. Bull JJ, Crandall C, Rodriguez A, Krone SM. Models for the directed evolution of bacterial allelopathy: bacteriophage lysins. PLoS 2015;3:1679.
32. Weitz JS, Hartman H, Levin SA. Coevolutionary arms races between bacteria and bacteriophage. Proc Natl Acad Sci U S A. 2006;7:8.
33. Karolakovsky AE, Wolf YI, Koonin EV. Immunity, suicide or both? Ecological determinants for the combined evolution of anti-pathogen defense systems. BMC Evol Biol. 2015;15:43.
34. Lashin SA, Matushkin YG. Haploid evolutionary constructor: new features and further challenges. In Silico Biol. 2012;11:125–35.
35. Lashin SA, Klimenko AI, Mustafin ZS, Kolchanov NA, Matushkin YG. HEC 2.0: improved simulation of the evolution of prokaryotic communities. Math Biol Bioinform. 2014;9:585–96.
36. Scheffer M, Baveco JM, DeAngelis DL, Rose KA, van Nes EH. Super-individuals a simple solution for modelling large populations on an individual basis. Ecol Modell. 1995;80:161–70.
37. Hellweger FL, Bucci V. A bunch of tiny individuals—Individual-based modeling for microbes. Ecol Modell. 2009;220:8–22.
38. Klimenko AI, Matushkin YG, Kolchanov NA, Lashin SA. Modeling evolution of spatially distributed bacterial communities: a simulation with the haploid evolutionary constructor. BMC Evol Biol. 2015;15:53.
39. Ptashne M. A genetic switch: Gene control and phage. lambda. Elsevier B.V., 1986.
40. Lashin SA, Matushkin YG, Suslov VV, Kolchanov NA. Computer modeling of genome complexity variation trends in prokaryotic communities under varying habitat conditions. Ecol Modell. 2012;224:124–9.
41. Steward GF, Smith DC, Azam F. Abundance and production of bacteria and viruses in the Bering and Chukchi Seas. Mar Ecol Prog Ser. 1996;131:287–300.
42. France SC, Hessler RR, Vrijenhoek RC. Genetic differentiation between spatially-disjunct populations of the deep-sea, hydrothermal vent-endemic amphipod Ventrella sulfuris. Mar Biol. 1992;114:551–9.
43. Gavrilets S, Li H, Vose MD. Patterns of parapatric speciation. Evolution (N Y). 2000;54:1126–34.
44. Won Y, Young CR, Lutz RA, Vrijenhoek RC. Dispersal barriers and isolation among deep-sea mussel populations (Mytilidae: Bathymodiolus) from eastern Pacific hydrothermal vents. Mol Ecol. 2002;12:169–84.