Neutrino nucleus reactions within the GiBUU model

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Abstract. The GiBUU model, which implements all reaction channels relevant at medium neutrino energies, is used to investigate the neutrino and antineutrino scattering on iron. Results for integrated cross sections are compared with NOMAD and MINOS collaborations data. It is shown, that final state interaction can noticeably change the spectra of the outgoing hadrons. Predictions for the MINERνA experiment are made for pion spectra, averaged over NuMI neutrino and antineutrino fluxes.

1. Introduction
Neutrino and antineutrino scattering on nuclei for neutrino energies above 30 GeV was studied in several experiments starting from the 80s. Theoretically they were successfully described within the quark parton model as Deep Inelastic Scattering (DIS) processes. Recent measurements by MINOS and NOMAD collaborations also covered the intermediate energy region. Here the neutrino reactions are not so easy to model, because of the overlapping contributions from QE scattering, resonance production and background processes. This requires complex approaches that take all of the relevant channels into account.

Nuclear effects in neutrino reactions can also be studied in detail nowadays. The MINERνA experiment intends to perform measurements on Plastic (CH), Iron, Lead, Carbon, Water and liquid Helium targets in the NuMI beam, which would directly allow to compare nuclear effects on various nuclei. Besides muon detection, this experiment will also be able to resolve various final states by identifying the tracks of the outgoing hadrons. Theoretical modelling of such exclusive reactions requires realistic approaches to the description of the initial and final state interactions in target nuclei.

Both these requirements are satisfied by the GiBUU transport model [1, 2], which we use here to study neutrino and antineutrino scattering on iron. Our results are compared with the recent MINOS and NOMAD collaborations data. Predictions are also made for the spectra of the outgoing particles. The calculations are done without any fine tuning to the data covered here with the default parameters as used in the GiBUU framework.

2. GiBUU transport model
The GiBUU model was initially developed as a transport model for nucleon-, nucleus-, pion-, and electron- induced reactions from some hundreds MeV up to tens of GeV. Several years ago neutrino-induced interactions were also implemented for the energies up to a few GeV. Recently the code was extended to describe also the DIS processes in neutrino reactions. Thus, we can study all kind of elementary collisions on all kind of nuclei within a unified framework.
The model is based on well-founded theoretical ingredients and has been tested against various nuclear reactions. For a detailed review of the GiBUU model see [2].

GiBUU describes all processes relevant at medium energies, the cross section is calculated as
\[ \sigma_{\text{tot}} = \sigma_{\text{QE}} + \sigma_{\text{RES}} + \sigma_{\text{BG}} + \sigma_{\text{DIS}}. \]
Our approach to quasielastic (QE) scattering, resonance (RES) production and background (BG) processes is described in [3, 4]. The DIS scattering is included as PYTHIA simulation.

In the region of the shallow inelastic scattering, that is at moderate invariant masses, \( 1.6 \text{ GeV} < W < 2.0 \text{ GeV} \), there is a potential problem of double counting. Here the same physical events can be considered as originating from decays of high mass baryonic resonances or from DIS. In the GiBUU code we use the ansatz, that both RES, BG and DIS processes contribute in this region. While the RES and BG contributions are smoothly switched off in this region and DIS contribution is switched on. In essence, the DIS processes at \( W < 2 \text{ GeV} \) account for the resonances whose electromagnetic properties are not known and for the non-resonant processes giving several mesons in the final state beyond the one pion background. With this choice, the DIS events become noticeable at neutrino energies around 3 GeV.

3. Integrated cross sections.

As it was measured in 80s, the DIS cross section grows linearly with energy. So at high neutrino energies the data are conveniently presented as cross section per energy \( \sigma_{\text{tot}}/E_{\nu} \).

Despite the measurements being made on nuclear targets, the world average values are given [5] for isoscalar target: \( \sigma_{\text{tot}}/E_{\nu}(\nu) = 0.667 \pm 0.014 \cdot 10^{-38} \text{ cm}^2/\text{ GeV} \) for neutrinos and \( \sigma_{\text{tot}}/E_{\bar{\nu}}(\bar{\nu}) = 0.334 \pm 0.008 \cdot 10^{-38} \text{ cm}^2/\text{ GeV} \) for antineutrinos. Such an approach is meaningful, only if nuclear corrections are neglected.

![Figure 1](image.png)

**Figure 1.** Total cross section per nucleon for neutrino (left) and antineutrino (right) induced reactions on iron target. Various prescriptions to include nuclear effects in DIS are compared. MINOS collaboration data (○) are from [6, 7], IHEP-JINR collaboration data (♦) are from [8].

The actual value of such corrections for neutrino reactions is not known so far, because of both experimental inaccuracies and difficulties in the theoretical description. On one hand, nuclear parton distributions, based on electromagnetic scattering data and intended for description of both charged lepton and neutrino reactions, were introduced. For a review and a list of recent parametrizations see, for example, [9]. On the other hand, recent investigations [10, 11] showed, that in neutrino reactions nuclear corrections to parton distributions are at the same level as for electrons, but have a very different dependence on the Bjorken \( x \) variable. The topic remains controversial, with the hope that future precise MINERνA collaboration results on various targets will clarify the situation.
As we already mentioned, the GiBUU code uses PYTHIA for the simulation of DIS processes. In the GiBUU simulation the neutrino interacts with one initial nucleon, bound in the hadronic potential and having nonzero Fermi momentum. In order to be able to use the PYTHIA event simulator, we have to provide some quasi-free kinematics as inputs to PYTHIA. Various prescriptions to do this result in a $3 - 4\%$ difference in the results. The corresponding cross sections (denoted as “F-NO”, “F-CM”, “F-THRE”) are shown in Fig 1. Nuclear parton distribution functions from [12] are also implemented as one of the options to use (to avoid double counting, nuclear potential and Fermi motion in such calculations are switched off). The result (“nuclearPDF”) as well as the free cross section for iron composition (“26p+30n”) are also shown in Fig 1. At the moment we consider the various prescriptions mentioned above as intrinsic uncertainty of the GiBUU code, reflecting the lack of our understanding of the nuclear effects. No other event generator, as far as we know, accounts for nuclear corrections in high–energy neutrino reactions.

Fig. 1 shows, that our calculations are in a good agreement with the recent neutrino data, which are also consistent with each other. This figure shows that the decreasing slope of our curves for the neutrino cross section is in agreement with that of the data. This slope is not taken into account in deriving the world-average value, where it was assumed to be negligible. For antineutrino the agreement is good for $E_{\bar{\nu}_\mu} > 25$ GeV. For lower energies our curve is above the recent MINOS collaboration data, but below the IHEP-JINR results [8]. The overall agreement of our calculations with the data is therefore better than the agreement of the data with each other.

4. Final state interactions and change of the final hadronic spectra.
After being produced in the initial interaction, outgoing hadrons propagate throughout the nucleus. In GiBUU this process of final state interactions (FSI) is modeled by solving the semiclassical Boltzmann-Uehling-Uhlenbeck equation. It describes the dynamical evolution of the phase space density for each particle species under the influence of the mean field potential, introduced in the description of the initial nucleus state. Equations for various particle species are coupled through this mean field and also through the collision term. This term explicitly accounts for changes in the phase space density caused by elastic and inelastic collisions between particles. FSI decrease the cross sections as well as significantly modify the shapes of the final particle spectra. Such change was seen, for example, in photo-pion production [13] and is described by the GiBUU with a good accuracy. A similar change should be observed in neutrino reactions.

Fig. 2 shows the $\pi^+$ (left panels), $\pi^0$ (middle panels) and $\pi^-$ (right panels) spectra for neutrino (upper panels) and antineutrino (lower panels) NuMI fluxes for 1-pion events. Since MINOS [14] collaboration considered only events with the energy of the outgoing muon $E_{\mu} > 1.5$ GeV, we apply the same cut in our calculations. The green dashed lines show the kinetic energy ($T_\pi$) distributions before FSI, i.e. of pions produced in the initial neutrino vertex. The solid red lines show the distributions after FSI, i.e. of pions that made it out of the nucleus. Such spectra can also be calculated for any other outgoing particles (protons, kaons, eta) for any predefined final state and should be measurable in MINERνA experiment.

For dominant channels ($\pi^+$ production for neutrino reactions and $\pi^-$ in antineutrino ones), the FSI decrease the cross section at $T_\pi > 0.2$ GeV. This is mainly explained by pion absorption through $\pi N \rightarrow \Delta$ following by $\Delta N \rightarrow NN$. Pion elastic scattering in the FSI also decreases the pion energy, thus depleting the spectra at higher energies and accumulating strength at lower energies. Thus, an increase of the cross sections is observed at $T_\pi < 0.15$ GeV; altogether this leads to a significant change of the shape of the spectra.

Scattering can also lead to pion charge exchange. For neutrino-induced reactions, the $\pi^+ n \rightarrow \pi^0 p$ scattering in the FSI is the main source of side–feeding for the $\pi^0$ channel, leading
to a noticeable increase of the $\pi^0$ cross section at low $T_\pi$. The inverse feeding is suppressed, because less $\pi^0$ than $\pi^+$ are produced at the initial vertex. The same mechanism of side feeding from dominant to sub-dominant channel through $\pi^- p \rightarrow \pi^0 n$ is working for antineutrino induced reactions.

For the least dominant channel ($\pi^-$ production for neutrino reactions and $\pi^+$ in antineutrino ones), the FSI (in particularly side feeding) represent the main source of the events observed; thus a dramatic FSI effect.

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Figure 2. Pion kinetic energy distributions for neutrino and antineutrino induced reactions for 1-pion production (one pion of a given charge and no other pions are produced). Calculations are for the NuMI low-energy mode neutrino/antineutrino fluxes.