Role of intraband dynamics in the generation of circularly polarized high harmonics from solids

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Recent studies have demonstrated that the polarization states of high harmonics from solids can differ from those of the driving pulses. To gain insights on the microscopic origin of this behavior, we perform one-particle intraband-only calculations and reproduce some of the most striking observations. For instance, our calculations yield circularly polarized harmonics from elliptically polarized pulses that sensitively depend on the driving conditions. Furthermore, we perform experiments on ZnS and find characteristics partly similar to those reported from silicon. Comparison to our intraband-only calculations shows reasonable qualitative agreement for a below-band-gap harmonic. We show that intraband dynamics predict depolarization effects that gain significance with higher field strengths and we observe such effects in the experimental data. For harmonics above the band gap, interband dynamics become important and the high-harmonic response to elliptical excitation looks systematically different. Our work proposes a method to distinguish between different high-harmonic generation mechanisms and it could pave the way to compact solid-state high-harmonic sources with controllable polarization states.

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I. INTRODUCTION

High-harmonic generation (HHG) is a highly nonlinear optical process in which many photons of an ultrashort laser pulse are upconverted to one photon of much higher energy. In atomic gases, where it was first discovered [1,2], this process is well described by a three-step model which takes into account ionization, subsequent acceleration of the free electron in the laser field, and recombination of the electron with its parent ion. In the last step, the acquired energy of the electron is emitted as a highly energetic photon [3]. The harmonic yield decreases strongly with elliptical driver polarization, which was early understood as an indication of the validity of the three-step model, because it precisely predicts the reduction of probability for the free-electron wave packet to return to its parent ion [4,5]. The harmonic yield vanishes with circularly polarized excitation and the generation of circularly polarized harmonics with other methods has evolved to a lively topic. Elaborate schemes for circularly polarized HHG have been presented, for instance HHG with counter-rotating circularly polarized bicolor pulses [6,7], with noncollinear counter-rotating circularly polarized pulses [8], and the combination of two orthogonal linearly polarized HHG beams with an appropriate phase shift [9].

In crystals [10,11] the simple recollision-physics picture of gas HHG does not hold. Here, electrons are never really free and their energy dispersion is given by the band structure of the solid target, which consists of many bands with different momentum-dependent curvatures and probabilities of transitions between the bands. Moreover, the Coulomb potential cannot be neglected, as the electrons travel in matter, and the single active electron approximation needs to be replaced by the assumption that electrons are independent particles, which is not always a good approximation, for instance in so-called strongly correlated materials [12].

The deviations of the band dispersion from the quadratic free-electron dispersion cause the electrons to move in a nonlinear fashion, thereby emitting higher frequency components than the fundamental driving field contains. This is a new type of HHG mechanism that cannot be found in HHG from gaseous atoms and is called the “intraband” mechanism. In contrast, the “interband” mechanism describes the radiation emitted upon transition from one band to another and is somewhat more similar to the emission of higher harmonics during the recombination step in gaseous atoms [11,13].

The response of solid-state HHG to elliptically polarized driving fields has been found to strongly differ from the atomic case. For instance, it has been demonstrated experimentally in MgO and graphene that the harmonic yield could be enhanced when changing from linear to elliptical driving polarization [14,15]. Subsequent works studied the polarization states of the emitted harmonics and found that circularly polarized harmonics can be generated from circularly [16–18] and elliptically [16,17] polarized single-color driving pulses. In the first case, the harmonics’ polarization states can be understood by a group-theoretical analysis leading to selection rules for each of the crystallographic groups, which was derived already 50 years ago [19]. The polarization states of

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the emitted harmonics driven by elliptically polarized fields, however, were shown to depend sensitively on the driving ellipticity and crystal rotation [16,17]. Moreover, they were intensity dependent and therefore directly dependent on the precise carrier dynamics [16,17]. All this is well reproduced with a time-dependent density functional theory description which includes the full band and crystal structure and does not require any a priori assumptions to match the experiments [17]. On the other hand, these calculations are costly and it is not always straightforward to extract an intuitive physical picture from these complex simulations.

In this work, we therefore attempt to isolate a single mechanism and study its consequences on the harmonics’ polarization states. Our aim is that this reduction to a simplified physical model will allow us to qualitatively understand the microscopic origin of some of the observed phenomena and that this will help in interpreting the obtained experimental results.

While both intra- and interband mechanisms are intrinsically coupled [20], it is understood that the interband mechanism only contributes for photon energies above the band gap and for a reasonably high joint density of states [21]. Because circularly polarized harmonics from elliptically polarized driving fields have also been demonstrated below the band gap and with a low joint density of states [17], we will focus our attention here on the intraband mechanism. Intraband-only calculations have been successfully utilized to reproduce the linear relationship of the cutoff energy to the driving field [10,22,23], the sixfold rotaional symmetry of HHG spectra in the threefold-symmetric crystal GaSe [24], and anisotropic HHG emission in ZnSe [25], as well as to reconstruct the band structure [26,27] and the Berry curvature [28] of SiO2. However, in solid-state HHG, simplified models that consider only intraband dynamics have so far not been used to study the effects of elliptical polarization. It is clear that such a model ignores influences from dephasing [29], wave packet spreading [16], HHG from multiple bands [30], contribution from holes [25], along with effects of the subcycle ionization dynamics [31].

We want to emphasize that the intraband mechanism was also used to model high-harmonic emission with the highest photon energies reported from solids to date (∼40 eV) [26]. Indeed, there are transparency regions in solids, for which the joint density of states (JDOS) goes to zero and interband recombination is not allowed as no pair of valence and conduction bands exists given such energy. In these regions, only intraband harmonics can appear, and our results should also apply there. So, even if we only discuss low-order harmonics in this work (to compare with our experimental data), our findings should be applicable to any interband-only generation of higher-energy photons, potentially enabling circularly polarized harmonics up into the extreme-ultraviolet (XUV) spectral region.

The rest of the paper is organized as follows. Having reviewed the theoretical and experimental methods in the next section, we present simulation results from a simple tight-binding-type band structure in Sec. III. In Sec. IV we present measurements on ZnS and compare these measurements to our calculations. Finally, we summarize the work and draw our conclusions in Sec. V.

II. METHODS

A. Theoretical model

Here we start by considering the dynamics of an electron wave packet in a single band. The current density \( \mathbf{j} \) at time \( t \) can be described as

\[
\mathbf{j}(t) = - \int_{\text{BZ}} e \mathbf{v}_k(t) n_k(t) d\mathbf{k}. \tag{1}
\]

Here, BZ refers to the first Brillouin zone, \( e \) is the electron charge, \( n_k \) is the charge distribution in \( \mathbf{k} \) space, and \( \mathbf{v}_k \) is the \( \mathbf{k} \)-dependent electron velocity. The latter consists of two terms, one of which is coined the anomalous velocity that contains the Berry curvature [32,33]. For the square lattice in Sec. III, the Berry curvature is zero because of symmetries and for ZnS in Sec. IV, we have confirmed that the influence of a band-averaged Berry curvature on the studied odd harmonic is negligible. To keep our discussion as simple as possible, we will therefore neglect the anomalous velocity term in this paper, which is in agreement with other recent works that utilized this model to study odd orders in solid HHG [24–27].

Assuming a fully localized electron wave packet at \( \mathbf{k}(t) \), i.e., \( n_k(t) = \delta(\mathbf{k} - \mathbf{k}(t)) \), and inserting the definition of the electron polarization (without the anomalous velocity term) \( \mathbf{v}_k = \frac{i}{\hbar} \frac{d\mathbf{k}}{dt} \), Eq. (1) simplifies to

\[
\mathbf{j}(t) = - \frac{e}{\hbar} \frac{d\mathbf{E}_k}{dt} |_{\mathbf{k}=\mathbf{k}(t)}. \tag{2}
\]

\( \mathbf{E}_k \) is the conduction band dispersion. Under these assumptions, the emitted electric field \( \mathbf{E}_{\text{HHG}}(t) \) originating from an intraband current is

\[
\mathbf{E}_{\text{HHG}}(t) \propto \frac{d\mathbf{j}(t)}{dt} = - \frac{e}{\hbar} \frac{d^2\mathbf{E}_k}{dt^2} |_{\mathbf{k}=\mathbf{k}(t)} = e^2 \left( \frac{1}{m_k^*} \right)_{\mathbf{k}=\mathbf{k}(t)} \cdot \mathbf{E}_L(t). \tag{3}
\]

\( \mathbf{E}_L(t) \) denotes the driving laser field. Furthermore, \( m_k^* \) is the effective mass tensor. Here we have used the acceleration theorem \( k(t) = -\frac{e}{\hbar} \int_0^t \mathbf{E}_L(t') dt' \) and with it the assumption that the electron is initially located at the \( \Gamma \) point. Finally, the emitted high-harmonic spectrum can be calculated as

\[
I_{\text{HHG}}(\omega) \propto |\text{FT}[\mathbf{E}_{\text{HHG}}(t)]|^2. \tag{4}
\]

It can be seen from Eq. (3) that the nonlinear evolution of \( \frac{d^2\mathbf{E}_k}{dt^2} \) is the source for nonperturbative emission of higher-frequency content. When happening in repetition over multiple laser cycles, this emission consists of high harmonics of the driving laser frequency [10,20].

In the following discussion we will consider the light components with respect to the polarization ellipse, i.e., \( \mathbf{E}_\parallel \) and \( \mathbf{E}_\perp \). Whenever we discuss harmonic order \( n \) or the corresponding electric field \( \mathbf{E}_n \), we have band-pass-filtered the Fourier transform of the total electric field in a window of \( nf \pm 0.3f \), where \( f \) is the center frequency of the driving field and \( n \) is the harmonic order. We checked that defining the harmonic response by taking only the response at the center value of the harmonic peak, or by averaging over an energy range, does not affect our conclusions. By finding the axes of minimum
(\alpha_{\text{min}}) and maximum (\alpha_{\text{max}}) harmonic yield \( I_n \), we calculate the harmonic ellipticity as

\[ |\epsilon_n| = \sqrt{I_n(\alpha_{\text{min}}) / I_n(\alpha_{\text{max}})}. \]

This approach resembles the experimental method to rotate a polarizer in order to determine \(|\epsilon_n|\). In our simulations, we use the driving field

\[ E_L(t) = \frac{\bar{E}(t)}{\sqrt{1 + \epsilon^2}} \left( \cos(\omega t) \right), \]

where \( \bar{E}(t) \) is a Gaussian envelope with a FWHM pulse duration of 70 fs and a central wavelength of 2100 nm. The field is rotated by an angle \( \theta \) by multiplying \( E_L \) with the rotation matrix. Throughout this paper we keep the driving field strength below the threshold above which Bloch oscillations appear. This is compatible with experimental conditions for this driving wavelength [17].

DFT calculations for bulk ZnS were performed with the Octopus code [34–37], using a lattice parameter of 5.41 Å, norm-conserving pseudopotentials, and a real-space grid spacing of 0.25 bohrs. We used a sampling of 21×21×21 \( k \) points to sample the Brillouin zone and we approximated the spacing of 0.25 bohrs. We used a sampling of 21 norm-conserving pseudopotentials, and a real-space grid.

Importantly, we measure the harmonics’ ellipticity as

\[ \text{DoP} = \frac{\sqrt{S_1^2 + S_2^2 + S_3^2}}{S_0}, \quad \text{DoP} \in [0, 1]. \]

As stated above, in experiment, a Fresnel rhomb is inserted for the measurement of \( S_3 \). For the simulations we multiply the electric field of a given harmonic with the Jones matrix of a QWP and the Jones matrix of a polarizer with the angle \( \phi_{\text{pol}} \). The hereby transmitted field is integrated over time which equals the experimental detection method.

### III. Square Lattice

First we will discuss a two-dimensional tight-binding band structure

\[ E_k = \frac{\hbar^2}{4a^2m_e} \left\{ 1 + \sum_m c_m [\cos(mk_xa) + \cos(mk_ya)] \right\}. \]

We set all \( c_m \) zero except for \( c_1 = -0.95 \) and \( c_3 = -0.05 \). These coefficients have previously been used in the one-dimensional case to theoretically model HHG from ZnO with intraband dynamics alone [10]. We use a lattice constant of \( a = 5.4 \) Å.

Equation (13) describes a square lattice. We call the axes parallel to \( k_x \) and \( k_y \), \( \Gamma X \) and the ones rotated by 45° \( \Gamma K \). The peak electric field is 2 V/nm. Figure 1(a) shows the calculated high-harmonic spectra with linear polarization along \( \Gamma X \) and \( \Gamma K \). With this band structure and our driving conditions, the harmonic signal is maximized along \( \Gamma X \), where harmonics are generated up to the 11th order (HH11). Along \( \Gamma K \), the overall harmonic yield is lower and also the cutoff is reduced. Figure 1(b) (bottom panel) depicts the perpendicular and parallel components of HH5 and HH9 versus crystal rotation angle. The signal is fourfold symmetric, as expected from a cubic structure. For polarization along the symmetry axes, the emitted field is completely parallel to the driving field. However, for sample rotations between 0° and 45°, the emitted harmonic fields contain a small perpendicular component. This is a consequence of different band curvatures along the \( x \) and \( y \) components of the driving field [Eq. (3)]. Because in this case the respective relative phases \( \varphi \) [top panel of Fig. 1(b)] are close to 0 for all sample rotations, the emitted fields stay linearly polarized [center panel of Fig. 1(b)] but are rotated with respect to the driving field. A behavior similar to this has already been observed experimentally [17,40].

Figure 1(c) shows the temporal evolution of \( E_x \) and \( E_y \) with a driver ellipticity \( \epsilon = 0.15 \) and major axis along \( \Gamma K \).
Only an excerpt of the rising edge of the pulse is shown; the highest field strength is reached at 0 fs. Although the perpendicular component is much weaker due to the low ellipticity of the driving field, it shows nonsinusoidal behavior starting at around −70 fs which is earlier than the parallel component, where clear nonsinusoidal components start to arise only at around −50 fs. This illustrates how the high harmonics can have totally different polarization states than the driving field.

The harmonics’ behavior for the same driving ellipticity $\epsilon = 0.15$ as a function of the crystal rotation angle is depicted in Fig. 1(d). Now the relative phases between $E_\| \parallel$ and $E_\perp \perp$ evolve in a more complicated way, reaching $90^\circ$ along $\Gamma K$. Hence, the ellipticities [center panel of Fig. 1(d)] peak for this sample rotation. HH5 becomes circularly polarized while HH9 exhibits only little ellipticity. For excitation away from a major symmetry axis, the fields are again rotated with respect to the driving laser. In summary, the harmonics’ polarization states differ among individual harmonics and sensitively depend on the crystal rotation and the driving ellipticity.

Importantly, our results show that pure intraband dynamics are sufficient to produce circularly polarized harmonics from elliptically polarized driving pulses, as we have observed experimentally from Si [17].

Next, we extend the analysis of the harmonics’ polarization states by varying the driving ellipticity further. Figures 2(a) and 2(b) show the evolution of HH5’s polarization versus driving ellipticity along $\Gamma K$ (a) and $\Gamma \Gamma$ (b). As discussed above, $\Gamma X$ is the direction to most efficiently generate harmonics. To drive the electrons away from that axis with an introduced ellipticity means—at least for this simple band structure—to generate harmonics less efficiently. The total harmonic yield therefore decreases [bottom panel of Fig. 2(a)] with very little rise of the perpendicular component. Hence, although the relative phase (top panel) is $90^\circ$ for most driver ellipticities, the harmonic ellipticity is low. For circular excitation HH5 becomes also circular. In fact, all harmonics become circular for circular excitation, and we even find that our simple model predicts that subsequent harmonics have alternating helicities, which is required by selection rules for cubic materials [19] and was recently confirmed experimentally [17,18].

When the driving major axis is set along $\Gamma K$ [Fig. 2(b)], harmonics are generated least efficiently. As a consequence, the perpendicular component increases strongly with small ellipticity values [bottom panel of Fig. 2(b)]. At $\epsilon = 0.17$, $E_{\perp \perp}$ and $E_{\perp \perp}$ have the same magnitude and—because $|\psi|$ is $90^\circ$—HH5 becomes circularly polarized (center panel). Further increase of the driving ellipticity causes $E_{\perp \perp}$ to dominate, which rotates the harmonics’ major axis by $90^\circ$. When the perpendicular component peaks, conditions are reversed and the parallel component rises again. Note that the relative phase is flipped in this case, which reverses the helicity of the harmonics’ polarization ellipse. The ellipticity of HH5 peaks again at $\epsilon = 0.55$ and $E_{\perp \perp}$ dominates for even more elliptically polarized drivers. At circularly polarized excitation, HH5 becomes circular once again. Qualitatively, we have observed very similar behavior to this in Si (compare Figs. 4 and S10 in Ref. [17]).

For polarization along this axis $\Gamma K$, the total yield of HH5 stays constant for all driver ellipticities. We would like to emphasize that—contrary to HHG from atomic gases—the intraband mechanism does not necessarily predict the harmonic yield to decrease with increasing ellipticity. The harmonic yield is a sole consequence of the band curvatures at different k values which can even be higher for elliptical polarization. Similar harmonic yields for linear and circular excitation have been reported in SiO$_2$ [17] and GaSe [18] with mid-infrared excitation. Interband transitions, however, will be reduced with elliptically polarized fields because the peak electric field is reduced by $E_{\text{eff}} / E_{\text{lin}} = \sqrt{1/(1 + \epsilon^2)}$. 

FIG. 1. (a) Spectra along the major symmetry axes $\Gamma X$ and $\Gamma K$ ($\epsilon = 0$). (b) Top panel: Relative phase $\phi$ between $E_\parallel$ and $E_\perp$ of HH5 and HH9; center panel: respective harmonic ellipticities $\epsilon$; bottom panel: individual intensity components of HH5 and HH9 parallel and perpendicular polarized to the driving field for different sample rotations ($\epsilon = 0$). (c) Excerpt of the emitted electric field components parallel and perpendicular to the driving major axis along $\Gamma K$ ($\epsilon = 0.15$). (d) Same as (b) but with $\epsilon = 0.15$.

FIG. 2. (a), (b): Ellipticity-dependent relative phases between $E_{\perp \perp}$ and $E_{\perp \perp}$ (top panel), corresponding ellipticities (center panel), and intensities of parallel and perpendicular components of HH5 along $\Gamma X$ (a) and $\Gamma K$ (b) (bottom panel). Ellipticities of HH5 (c) and HH9 (d) in dependence on sample rotation and driver ellipticity. $0^\circ$ and $90^\circ$ refer to $\Gamma X$, $45^\circ$ and $135^\circ$ to $\Gamma K$. 

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Therefore, fewer conduction-band electrons should contribute to the HHG current. But even here the effect on the harmonic yield is unclear, because fewer electrons could also cause less dephasing to happen and thereby increase the harmonic yield. All this should depend on the exact driving conditions and the band structure and is not exactly understood at this point.

Figures 2(c) and 2(d) depict the full polarization maps of HH5 and HH9 versus driving ellipticity and sample rotation. The previous discussion is summarized in these plots. The conditions of high |\(\epsilon_n|\) are seen as “islands” along \(\Gamma K\). For higher harmonics, these islands are more sensitive to the exact driving conditions and more islands appear. Qualitatively, this is what has been observed in Ref. [17]. For other sample rotations, the harmonics stay largely linearly polarized due to a small relative phase between \(E_\perp\) and \(E_\parallel\). However, they are often rotated with respect to the driving field (not shown). As required for a cubic system, all harmonics become circularly polarized for \(\epsilon = 1\) independently of the sample rotation.

IV. ZINC SULFIDE

After having studied a simple model band structure, we can address a real material and compare our simulation results with measurements. We have chosen to investigate 50-µm-thin, (100)-cut ZnS, because its lower conduction band is well isolated from the others and therefore our one-band model could constitute a reasonable approximation. Since harmonics below the band gap should be produced predominantly by intraband dynamics [21], we will focus our attention in the following on HH5. For our peak electric field strength, the harmonics are generated nonperturbatively, as we have confirmed by studying harmonics’ yield versus driving field strength [10]. In the simulations, unless otherwise noted, we use the same peak electric field strength as in the experiment, i.e., 1 V/nm. The band structure of ZnS has been constructed as described in Sec. II.A.

ZnS has a zinc-blende crystal structure and, hence, is not inversion symmetric. In the experimental harmonic spectra, the lack of inversion symmetry manifests itself in the generation of even-order harmonics. Because the single-band model employed in this work cannot produce even harmonics [24,28], we will investigate here only the odd harmonics.

Before investigating the harmonic ellipticities, let us first consider the yield of HH5 and compare experimental to simulated data in dependence on the driving ellipticity and sample rotation [Figs. 3(a) and 3(b)]. Due to the zinc-blende crystal structure, neither the experimental nor the calculated data show a fourfold symmetry. Furthermore, it is apparent that the yield behaves distinctly differently from the monotonic behavior that is known from gas HHG. This is true for both the experimental and the simulated results. The simulation reproduces the two minima of the harmonic yield well and also parts of the regions where the yield is maximized. However, around the region of \(\epsilon \approx 0.4\) and \(50^\circ < \theta < 100^\circ\) some differences can be seen.

Figures 3(c) and 3(d) show the measured and calculated \(|\epsilon_5|\) for the same driving conditions as above. A somewhat peculiar aspect of this crystal structure is that harmonics are elliptically polarized with circular excitation. This is required by selection rules for the zinc-blende symmetry group [19] and is confirmed in both our experimental data and calculations. For elliptical excitation, we once again find islands of high \(|\epsilon_n|\), both in the simulated as well as in the measured data. Some features of the experimental data are qualitatively well reproduced in the simulations. This is especially true for the asymmetric elongated island around \(\epsilon \approx 0.8\) and \(110^\circ < \theta < 150^\circ\). Also the two islands along \(\theta \approx 45^\circ\) can be found both in experiment and simulations. The experiments show a circularly polarized HH5 for \(\epsilon \approx 0.6\), \(\theta \approx 80^\circ\) which is not covered in the simulation. Also the shape of the islands around \(\theta = 45^\circ\) are not perfectly reproduced. It can be expected that electron-electron interactions and the influence of harmonic emission due to electrons that are promoted to the conduction band at different times have a great effect on these kinds of maps [31]. Also hole dynamics can be expected to play a role [25]. Discrepancies in such a side-by-side analysis are therefore not surprising when these effects are neglected. When comparing the ellipticity maps to the maps of the harmonic yields [Figs. 3(a) and 3(b)], it is interesting to note that most of the peaks of \(|\epsilon_5|\) happen closely to the minima of the harmonic yield. This is not true for the peak around \(\epsilon \approx 0.6\) and \(\theta \approx 80^\circ\), which does not appear in the simulation results.

For harmonics above the direct band gap, the assumption that intraband dynamics alone underlie high-harmonic emission breaks down. We can observe this in ZnS by studying...
As shown for zinc-blende ZnS in simulated data for certain driving conditions, depolarization effects that appear both in experimental and theoretical scenarios suggest that intraband dynamics alone already produce circularly polarized high harmonics with elliptically polarized excitation. Experimentally, after having demonstrated this behavior in silicon [17], we have shown that this is the case by increasing the peak electric field strength. Figures 4(c) and 4(d) compare the simulated DoP for the field strength used so far, 1 V/\mu m, and a higher field strength of 1.3 V/\mu m. Depolarization is clearly more prominent for the latter. In the case of the higher field strength, HH5 can even be slightly depolarized with linear driving polarization. We could not conduct the measurements at higher field strengths due to laser-induced damage in that case. However, this should be possible with shorter pulses or other materials. Note that depolarization effects have been discussed recently in gas HHG [42] and we show here that the influence of the band structure can cause additional depolarization effects in solid HHG.

V. CONCLUSION

We have demonstrated that simple intraband dynamics alone produce salient features in the polarization of HHG from solids that can also be found in experimental results. Striking are the appearances of circularly polarized harmonics with elliptically polarized excitation as well as deviations of the harmonics’ major axis with respect to the driving major axes. Experimentally, after having demonstrated this behavior in cubic Si for the first time [17], we have shown here that zinc-blende ZnS is another material from which one can produce circularly polarized high harmonics with elliptically polarized excitation. This suggests that this is a fundamental response of solid HHG to elliptical excitation and that it can be found in a much broader range of excitation conditions and crystals. We have discussed effects of depolarization that can result from intraband dynamics alone and have demonstrated this both in experiments and simulation. According to the intraband mechanism, depolarization effects are expected to become more significant for higher field strengths. We have also demonstrated differences in the polarization-state-resolved response of high harmonics above the band gap, where the interband mechanism cannot be neglected. Previously, the intraband-only model was used to successfully...
reproduce the XUV spectra up to record 40 eV photon energy from quartz [26]. In consequence, we predict that the island-like circularly polarized harmonics from elliptically polarized driving pulses can also be found in this spectral region. This could pave the way to relatively compact sources of circularly polarized XUV radiation. Furthermore, the direct link of intraband dynamics to solid HHG could allow for k-resolved tracking of the fastest oscillating currents that ultrafast laser pulses can generate in solids to date.

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