VELOCITY DISPERSION PROFILE OF THE MILKY WAY HALO

WARREN R. BROWN1, MARGARET J. GELLER1, SCOTT J. KENYON1, AND ANTONALDO DIAFERIO2,3
1 Smithsonian Astrophysical Observatory, 60 Garden St., Cambridge, MA 02138, USA; wbrown@cfa.harvard.edu, mgeller@cfa.harvard.edu, skennon@cfa.harvard.edu
2 Dipartimento di Fisica Generale “Amedeo Avogadro,” Università degli Studi di Torino, Via P. Giuria 1, I-10125 Torino, Italy
3 Istituto Nazionale di Fisica Nucleare (INFN), Sezione di Torino, Via P. Giuria 1, I-10125, Torino, Italy; diaferio@ph.unito.it

ABSTRACT

We present a spectroscopic sample of 910 distant halo stars from the Hypervelocity Star survey from which we derive the velocity dispersion profile of the Milky Way halo. The sample is a mix of 74% evolved horizontal branch stars and 26% blue stragglers. We estimate distances to the stars using observed colors, metallicities, and stellar evolution tracks. Our sample contains twice as many objects with $R > 50$ kpc as previous surveys. We compute the velocity dispersion profile in two ways: with a parametric method based on a Milky Way potential model and with a non-parametric method based on the caustic technique originally developed to measure galaxy cluster mass profiles. The resulting velocity dispersion profiles are remarkably consistent with those found by two independent surveys based on other stellar populations: the Milky Way halo exhibits a mean decline in radial velocity dispersion of $-0.38 \pm 0.12$ km s$^{-1}$ kpc$^{-1}$ over $15 < R < 75$ kpc. This measurement is a useful basis for calculating the total mass and mass distribution of the Milky Way halo.

Key words: Galaxy: halo – Galaxy: kinematics and dynamics

Online-only material: color figure, machine-readable and VO tables

1. INTRODUCTION

A fundamental property of the Milky Way galaxy is its total mass. In the cold dark matter paradigm, the total mass of a galaxy’s dark matter halo correlates with its merger history, star formation history, and number of its satellite sub-halos. A galaxy’s mass distribution is also a fundamental constraint on theories. Cold dark matter models predict that density follows a universal Navarro–Frenk–White (NFW) profile (Navarro et al. 1997); in Modified Newtonian Dynamics there is no dark matter halo and the mass distribution is highly flattened compared to cold dark matter models (Hernandez et al. 2009). The Milky Way provides a unique laboratory for testing these issues. Nevertheless, the mass and mass distribution of the Milky Way are among the most poorly known of all Galactic parameters, especially at large distances $R \gtrsim 50$ kpc. Total mass estimates span at least a factor of 4, from $0.5 \times 10^{12}$ to $2 \times 10^{12} M_\odot$ (see below). Recent theoretical work based on semi-analytic models and timing arguments suggest that the Milky Way may be even more massive (Li & White 2008; Abadi et al. 2009). Clearly, the mass and mass distribution of the Milky Way remain controversial and important issues.

A powerful approach for measuring the Milky Way’s mass distribution is measuring the motions of tracer objects. Radio masers probe the Galactic rotation curve out to 15 kpc (Reid et al. 2009); H$_2$ gas probes the rotation curve to larger distances (Kalberla & Dedes 2008). Luminous tracers at $R \gtrsim 50$ kpc, however, are rare. Historically, globular clusters and dwarf galaxies were used to measure the total mass of the Milky Way (e.g., Little & Tremaine 1987; Zaritsky et al. 1989; Kallio & Lynden-Bell 1992; Kochanek 1996; Wilkinson & Evans 1999). These mass estimates were based on samples of a few dozen objects, and suffered from a systematic factor of $\sim 2$ uncertainty depending on the inclusion of Leo I. Post-main-sequence halo stars provide denser tracers, but the blue horizontal branch (BHB) star samples of Sommer-Larsen et al. (1997) and Sakamoto et al. (2003) are limited to $R \lesssim 20$ kpc. Battaglia et al. (2005) added 58 distant red giants from the Spaghetti survey and claimed a large decline in the velocity dispersion at $R > 50$ kpc. Recently, Xue et al. (2008) analyzed the Sloan Digital Sky Survey (SDSS) sample of 2466 BHB stars and found a small decline in velocity dispersion with distance. Only 80 of the SDSS BHB stars are located at $R > 50$ kpc.

Here, we use the distant halo stars from the hypervelocity star (HVS) program (Brown et al. 2005a, 2006a, 2006b, 2007b, 2007c, 2009a, 2009b) to measure the velocity dispersion profile of the Milky Way. Our data set is a complete spectroscopic sample of 910 stars observed over 7300 deg$^2$ of the SDSS Data Release 6 imaging region. We gain increased leverage on the velocity dispersion profile for $R \gtrsim 50$ kpc. We find an average decline in radial velocity dispersion of $0.38 \pm 0.12$ km s$^{-1}$ kpc$^{-1}$ over $15 < R < 75$ kpc.

In Section 2, we describe the observations and luminosity estimates for stars in our sample. In Section 3, we make parametric and non-parametric estimates of the velocity dispersion profile. We also discuss possible systematic effects, and compare our results with earlier work. We conclude in Section 4. The data are in the Appendix.

2. DATA

The HVS program is a radial velocity survey of stars selected with the colors of late-B-type stars. The radial velocity survey is now 93% complete over 7300 deg$^2$ of the SDSS DR6 imaging footprint. Here, we focus exclusively on the stars with late-B and early-A spectral types; we exclude all white dwarfs (Kilic et al. 2007a, 2007b), B supergiants (Brown et al. 2007a), emission line galaxies (Kewley et al. 2007; Brown et al. 2008b), and quasars (Brown et al. 2009a).

The data set contains 910 stars: 571 stars from the original HVS survey (Brown et al. 2007c), 331 stars from the new HVS survey (Brown et al. 2009a), and 8 BHB stars from the earliest sample (Brown et al. 2005a). We begin by describing the observables—magnitude, position, velocity—all of which are well determined. Stellar luminosity is less well determined and must be inferred from colors and metallicity. We discuss
the luminosity estimates and distance determinations in some detail. The observed and derived quantities for each star are listed in Table 1, described in the Appendix.

2.1. Photometry

All photometry comes from SDSS Data Release 6 (Adelman-McCarthy et al. 2008). We use Uber-calibrated point-spread function (PSF) magnitudes, and correct the magnitudes and colors for reddening following Schlegel et al. (1998).

2.2. Target Selection

The HVS survey target selection emphasizes outliers in the halo population: we target stars redder in $(u - g)$ than known white dwarfs and bluer in $(g - r)$ than known BHB stars (Brown et al. 2006b). This color cut through the stellar population, illustrated in Figure 1, allows us to detect HVSs efficiently. The majority of targets, however, are normal halo stars.

Our target selection includes stars with $17 < g_0 < 19.5$ in the range $-0.39 < (g - r)_0 < -0.25$ (Brown et al. 2007c) and fainter stars with $19 < g_0 < 20.5$ over a broader color range $-0.40 < (g - r)_0 < -0.20$ (Brown et al. 2009a). We also include eight confirmed BHB stars from Brown et al. (2005a) with $19.5 < g_0 < 20.25$ and $-0.3 < (g - r)_0 < -0.1$. All 910 targets are located in the SDSS DR6 footprint and have an average surface density on the sky of $0.12$ deg$^{-2}$.

2.3. Radial Velocity

We obtained spectroscopic observations at the 6.5 m MMT telescope with the Blue Channel Spectrograph. We operated the spectrograph with the 832 line mm$^{-1}$ grating in second order, providing wavelength coverage 3650–4500 Å and a spectral resolution of 1.2 Å. We obtained all observations at the parallactic angle, with a comparison lamp exposure for every survey object.

We processed the data using IRAF in the standard way. We measure radial velocities by cross-correlating the observations with radial velocity standards (Fekel 1999) using the package RVSAO (Kurtz & Mink 1998). The average radial velocity uncertainty of the stars is ±12 km s$^{-1}$.

All velocities discussed here are in the Galacticocentric rest frame, indicated $v_{\text{rf}}$. Given the outer halo location of the stars, we note that the observed radial velocities are almost purely ($\sim$85\%) radial in the Galacticocentric frame. We transform heliocentric velocities ($v_{\text{helio}}$) into Galacticocentric rest-frame velocities assuming a circular velocity of 220 km s$^{-1}$ and a solar motion of $(U, V, W) = (10, 5.2, 7.2)$ km s$^{-1}$ (Dehnen & Binney 1998):  

$$v_{\text{rf}} = v_{\text{helio}} + 220 \sin l \cos b + (10 \cos l \cos b + 5.2 \sin l \cos b + 7.2 \sin b).$$  

(1)

Reid et al. (2009) argue for a larger circular velocity of 250 km s$^{-1}$ based on trigonometric parallaxes to star formation regions in the disk. We test using a circular velocity of 250 km s$^{-1}$ and find statistically identical velocity dispersion profiles. This insensitivity to circular velocity arises because the stars in our high latitude survey have a mean value of $|\sin l \cos b| = 0.32$; changing the Sun’s circular velocity by 30 km s$^{-1}$ results in a ±10 km s$^{-1}$ change in the stars’ rest-frame velocities. 10 km s$^{-1}$ is smaller than our measurement error and an order of magnitude smaller than the velocity dispersion of the stars. McMillan & Binney (2009) show that the Reid et al. (2009) data are consistent, at the 1σ level, with the canonical circular velocity of 220 km s$^{-1}$. Thus, we use 220 km s$^{-1}$ here.

Figure 2 plots the resulting Galactic rest-frame velocity distribution of the 910 halo stars. For reference, we also draw a Gaussian with zero mean and 106 km s$^{-1}$ dispersion (dotted line). The observations reveal a significant asymmetry of outliers in the tails of the velocity distribution. There are no stars with $v_{\text{rf}} < -300$ km s$^{-1}$ but 18 stars with $v_{\text{rf}} > +300$ km s$^{-1}$ (the HVSs). We address this issue in Section 3.

2.4. Metallicity

The strongest metal line in our spectra is the 3933 Å Ca$\text{ii}$ K line. Unfortunately, at the effective temperatures sampled by the survey, $10,000 \leq T_{\text{eff}} \leq 15,000$ K, the equivalent width of Ca$\text{ii}$ K is small (Wilhelm et al. 1999a). Thus, Ca$\text{ii}$ K provides poor leverage on the metallicity of our stars. Metallicity is better determined for redder (cooler) BHB stars, for example, the BHB survey of Brown et al. (2008a) and the BHB sample from the SDSS spectroscopic survey (Xue et al. 2008). The metallicity distributions of these two BHB samples are plotted in Figure 3 and are similar in shape. However, the outer halo sample of Xue et al. (2008) is about 0.2 dex more metal poor than the inner halo sample of Brown et al. (2008a). The mean metallicity of the Xue et al. (2008) BHB stars with $g_0 > 17$ is $[\text{Fe}/\text{H}]_{\text{Ca}} = -1.9$.

To make luminosity estimates, we assume that our survey stars have the metallicity distribution function of Xue et al. (2008). This assumption is reasonable given the very similar sky coverage and penetration into the halo of the two surveys: the stars occupy similar regions of the Milky Way halo. The reddest stars in our sample, where we can estimate metallicity, are metal poor (Brown et al. 2006b), consistent with the metallicity distribution function of Xue et al. (2008).

2.5. Spectroscopic Identification

Although the stars in our survey have the spectral types of late-B- and early-A-type stars, their nature is ambiguous. The old stellar population of the halo contains both evolved BHB stars and main-sequence blue stragglers. Halo surveys consistently find that ~50\% of A-type stars in the field are blue stragglers (Norris & Hawkins 1991; Kinman et al. 1994; Preston et al. 1994; Wilhelm et al. 1999b; Clewley et al. 2002, 2004; Brown et al. 2003, 2005b, 2008a; Xue et al. 2008). This result is problematic because BHB stars and blue stragglers can have very different luminosities (Figure 1). Spectroscopic measures of surface gravity can discriminate the evolutionary state of the stars (Kinman et al. 1994; Wilhelm et al. 1999a; Clewley et al. 2002, 2004). Unfortunately, surface gravity measures fail for our sample because BHB and main-sequence stars have nearly identical surface gravities at the effective temperatures of our stars.

We target stars so blue, however, that we largely exclude the possibility of blue stragglers. A $\pm 0.75 M_\odot$ star with $[\text{Fe}/\text{H}] = -1.9$ has a main-sequence lifetime of a Hubble time (Girardi et al. 2004). A field blue straggler cannot plausibly have more than twice the mass of a main-sequence turnoff star. In our sample, 36\% of the stars are bluer than both $(g - r)_0 = -0.27$ and $(u - g)_0 = 0.87$, the color of a 1.5 $M_\odot$ star with $[\text{Fe}/\text{H}] = -1.9$ (Girardi et al. 2004). Thus, the nature of many of the stars is clear: they are hot BHB stars.

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4 IRAF is distributed by the National Optical Astronomy Observatories, which are operated by the Association of Universities for Research in Astronomy, Inc., under cooperative agreement with the National Science Foundation.
Table 1
Data Table

| R.A. (hr) | Decl. (deg) | $g_0$ (mag) | $\sigma_g$ (mag) | $\sigma_{u-g}$ (mag) | $\sigma_{g-r}$ (mag) | $\sigma_{r-i}$ (km s$^{-1}$) | $v_{helio}$ (km s$^{-1}$) | $\sigma_v$ (km s$^{-1}$) | $l$ (deg) | $b$ (deg) | $v_{helio}$ (km s$^{-1}$) | $M_{L,BHB}$ (mag) | $\sigma_{BHB}$ (mag) | $R_{BHB}$ (kpc) | $M_{L,BH}$ (mag) | $\sigma_{BH}$ (mag) | $R_{BH}$ (kpc) | $J_{BHB}$ |
|----------|-------------|-------------|-----------------|---------------------|---------------------|-----------------------------|--------------------------|----------------------|----------|----------|--------------------------|-----------------|----------------|-----------------|-----------------|----------------|----------------|----------------|
| 00:02:05.713 | 31:18:50.23 | 20.434 | 0.026 | 0.778 | 0.095 | -0.277 | 0.040 | -209.3 | 14.0 | 110.717 | -30.385 | -34.3 | 1.17 | 0.24 | 68.7 | 2.19 | 0.33 | 42.2 | 0.70 |
| 00:02:33.817 | -9:57:06.85 | 18.434 | 0.021 | 0.753 | 0.040 | -0.328 | 0.040 | -87.7 | 9.7 | 86.763 | -69.316 | -14.8 | 1.31 | 0.12 | 33.9 | 2.06 | 0.24 | 26.2 | 0.29 |
| 00:04:36.491 | -9:57:19.48 | 19.834 | 0.018 | 0.922 | 0.103 | -0.167 | 0.032 | -172.6 | 35.0 | 87.977 | -69.584 | -100.7 | 0.69 | 0.17 | 75.3 | 2.83 | 0.27 | 35.2 | 0.33 |
| 00:05:28.141 | -11:00:10.07 | 19.141 | 0.042 | 1.007 | 0.081 | -0.275 | 0.047 | -115.9 | 10.9 | 86.890 | -70.586 | -47.8 | 0.94 | 0.13 | 44.6 | 2.51 | 0.19 | 22.9 | 0.64 |
| 00:07:52.013 | -9:19:54.32 | 17.302 | 0.017 | 1.016 | 0.036 | -0.276 | 0.039 | -114.5 | 9.9 | 90.855 | -69.443 | -42.2 | 0.91 | 0.11 | 26.3 | 2.53 | 0.16 | 16.5 | 1.00 |
| 00:12:26.890 | -10:47:54.56 | 18.898 | 0.025 | 1.006 | 0.064 | -0.321 | 0.038 | -128.2 | 10.5 | 91.741 | -71.269 | -62.8 | 0.94 | 0.12 | 42.4 | 2.52 | 0.18 | 22.9 | 0.67 |
| 00:23:53.294 | -1:04:46.40 | 18.199 | 0.016 | 0.749 | 0.042 | -0.255 | 0.025 | 19.7 | 9.8 | 107.552 | -63.125 | 109.0 | 1.15 | 0.17 | 30.7 | 2.22 | 0.26 | 21.1 | 0.82 |
| 00:29:31.158 | 15:39:40.20 | 19.069 | 0.024 | 1.057 | 0.069 | -0.270 | 0.038 | 22.3 | 35.0 | 115.201 | -46.881 | 153.4 | 0.88 | 0.12 | 51.2 | 2.56 | 0.18 | 27.8 | 0.53 |
| 00:36:40.570 | -11:11:25.02 | 17.421 | 0.018 | 0.778 | 0.028 | -0.304 | 0.031 | 32.5 | 9.8 | 109.940 | -73.689 | 84.1 | 1.26 | 0.12 | 21.6 | 2.09 | 0.22 | 16.6 | 0.89 |
| 00:39:06.749 | 24:09:05.62 | 19.348 | 0.018 | 0.948 | 0.081 | -0.255 | 0.030 | -130.0 | 35.0 | 119.332 | -38.634 | 15.0 | 0.94 | 0.14 | 41.4 | 2.49 | 0.21 | 17.3 | 0.55 |

(This table is available in its entirety in machine-readable and Virtual Observatory (VO) forms in the online journal. A portion is shown here for guidance regarding its form and content.)
Figure 1. Color–color diagram showing the distribution of the HVS survey stars (solid squares) and the Xue et al. (2008) BHB stars (dots) compared to lines of constant absolute magnitude $M_\odot$ for BHB stars (red lines, Dotter et al. 2008) and main-sequence stars (blue lines, Girardi et al. 2004). All tracks are for [Fe/H] = −1.9, the mean metallicity of halo stars. Dashed lines indicate the direction of increasing luminosity. At [Fe/H] = −1.9, BHB stars and blue stragglers share identical luminosities around $(u - g)_0 \approx 0.6$.

Figure 2. Distribution of velocities in the Galactocentric rest frame. The dotted line shows a fiducial Gaussian with zero mean and 106 km s$^{-1}$ dispersion. The positive velocity outliers with $v_{rf} > +400$ km s$^{-1}$ are the unbound HVSs.

Figure 3. Metallicity distribution function of inner halo BHB stars (Brown et al. 2008a) and outer halo BHB stars (Xue et al. 2008) based on Ca II K. The shift toward lower metallicity in the outer halo is expected; the Xue et al. (2008) BHB stars with $g_0 > 17$ have a mean [Fe/H]$_{Ca} = -1.9$.

2.6. Luminosity

We estimate luminosity from stellar evolution tracks. Girardi et al. (2002, 2004) provide main-sequence tracks in the SDSS passbands for metallicities ranging from solar to [Fe/H] = −2.3, but do not include the horizontal branch. Dotter et al. (2007, 2008) provide BHB tracks in the SDSS passbands over the same range of metallicities. To simplify the luminosity estimates, we fit low-order polynomials to the tracks as a function of both color and metallicity.

We estimate luminosity two ways, using a star’s $(u - g)_0$ and $(g - r)_0$ color. Our final luminosity is the weighted average of the two estimates. We weight by the slope of the observed $(u - g)_0$ versus $(g - r)_0$ distribution (Figure 1). This weighting is important because luminosity is most sensitive to $(u - g)_0$ at the blue end of our sample and to $(g - r)_0$ at the red end of our sample. The weighting favors luminosities derived from $(u - g)_0$ for $(g - r)_0 < -0.24$ and luminosities derived from $(g - r)_0$ for $(g - r)_0 > -0.24$. Figure 1 shows the resulting lines of constant luminosity for a star with $[\text{Fe/H}] = -1.9$ from the Girardi et al. (2004) main-sequence tracks (in blue) and from the Dotter et al. (2008) BHB tracks (in red).

The accuracy of the luminosity estimate depends on the accuracy of the stellar evolution models. For example, alpha-enhanced tracks (appropriate for the old stellar halo populations) are systematically bluer than solar-scaled tracks for both main-sequence and BHB stars (Lee et al. 2009).

The precision of the luminosity estimate is more robust because we apply the same tracks to all stars. The precision depends on observational uncertainties and is straightforward to quantify. A $g_0 = 19$ star at the median depth of our survey has uncertainties $\sigma_{(u-g)} = 0.05$ and $\sigma_{(g-r)} = 0.03$ in color and $\sigma_v = 12$ km s$^{-1}$ in velocity. We assume that metallicity is randomly drawn from the Xue et al. (2008) metallicity distribution function (Figure 3). We then propagate these uncertainties through the main-sequence and BHB
tracks to visualize the resulting distribution of luminosity estimates.

Figure 4 plots the distribution of luminosity and velocity (centered at zero) for two fiducial stars in the bluest quartile (left panel) and the reddest quartile (right panel) of the survey. Stars in the bluest quartile have luminosities precise to 10% because main-sequence and BHB stars have essentially identical luminosities at these colors (Figure 1). Stars in the reddest quartile, however, have bimodal luminosity distributions with a factor of 4 spread in luminosity (a factor of 2 in distance). This degeneracy is broken for confirmed BHB stars: 33 of our stars are listed as BHB stars in Xue et al. (2008) and 8 are BHB stars from our earliest sample (Brown et al. 2005a). For these confirmed BHB stars, we use only the BHB luminosity to calculate distance.

Three of the stars with $v_{rf} > +400$ km s$^{-1}$ in this survey are confirmed young main-sequence B stars (Fuentes et al. 2006; Bonanos et al. 2008; López-Morales & Bonanos 2008; Przybilla et al. 2008a, 2008b). For the purposes of this paper, however, we treat these HVSs the same as the other stars in our sample: we estimate distances to the HVSs as if they were halo BHB stars or metal-poor blue stragglers. We clip the HVSs from the sample when calculating the velocity dispersion in Section 3.

2.7. Distance

We calculate distances from the observed apparent magnitudes and estimated luminosities:

$$d = 10^{(g_0 - M_d)/5 - 2} \text{ kpc},$$

where $d$ is the heliocentric distance in kpc, $g_0$ is the apparent magnitude corrected for extinction, and $M_d$ is the absolute magnitude estimated above. We convert heliocentric distance $d$ to Galactocentric distance $R$ with the Sun at $R = 8$ kpc.

Figure 5 plots the resulting distance distribution of the survey stars compared with the Xue et al. (2008) sample of BHB stars. The Xue et al. (2008) sample contains more than twice as many stars as our sample; however, our sample is deeper and contains twice as many stars with $R > 50$ kpc. Neither sample fairly measures the density profile of the halo. The Xue et al. (2008) sample is incomplete in color, magnitude depth, and spatial coverage. Our sample is complete in all dimensions, but we find an artificially shallow density profile—consistent with

$$N(R) \propto R^{-2}$$

over the range $20 < R < 70$ kpc (Figure 5)—because we observe over a broader color range starting at $g_0 > 19$ mag. A shallow density profile works to our advantage for the velocity dispersion analysis, however, because our stars sample greater distances at a greater relative density.

3. HALO VELOCITY DISPERSION PROFILE

Based on the distances and velocities of the sample stars, we calculate the velocity dispersion profile of the Milky Way halo. We use two independent methods to calculate velocity dispersion: a parametric method based on a Milky Way potential model and a non-parametric method based on the Diaferio & Geller (1997) caustic technique, originally developed to measure galaxy cluster mass profiles. Using these two methods provides a measure of the systematic error introduced from clipping
velocity outliers. We also discuss the systematic error from binary stars and disk stars in our data set, and we conclude by comparing our velocity dispersion profiles with previous work.

3.1. Computational Approach

We use a Monte Carlo approach to model the distance to each star. We assume that photometric and velocity errors are Gaussian distributed, and that the underlying metallicity distribution is that of Xue et al. (2008). We then derive the luminosity for each star by randomly drawing its color and metallicity from the observed distributions and comparing them to the main-sequence and BHB tracks (Figure 1) described above. We sample the distributions 100 times per star. Using a Monte Carlo approach allows us to account for the non-Gaussian distribution of luminosity estimates unique to each star.

The resulting Monte Carlo catalog drawn from the observations produces the “cloud” of velocities and distances shown in Figure 6; the distribution of points reflects the uncertainties in the velocity measurements and the distance estimates of the stars.

We calculate the velocity dispersion profile by grouping stars into five or six unique bins in distance. The bins have sizes of 0.33$R$, chosen so that the bins contain at least 70 stars. We require 50 stars to obtain a dispersion with a formal statistical uncertainty of 10%. Bins with smaller occupation have dispersions systematically biased low resulting from small number statistics. Given the distance distribution of our sample, the occupation requirement constrains our velocity dispersion measurements to the region $15 < R < 75$ kpc. Stars with well determined luminosities contribute their full weight to a single distance bin; stars with poorly constrained luminosities contribute less weight distributed over multiple bins.

We use bootstrap re-sampling to calculate the uncertainty in the velocity dispersion measurement. Our procedure is to draw random sets of 910 stars, with replacement, from the Monte Carlo catalog and re-calculate the velocity dispersion. We resample 10,000 times; the uncertainty is the standard deviation of the velocity dispersions.

3.2. Velocity Dispersion: Potential Model

Our survey was designed to find unbound HVSs. Thus, the first step in calculating the velocity dispersion profile is to clip the unbound stars from the sample. Defining an unbound star is difficult, however. The best estimate of the Galactic escape velocity is $550 \pm 50$ km s$^{-1}$ at the solar circle, based on the highest velocity stars in the solar neighborhood (Smith et al. 2007). The escape velocity of the outer halo is more poorly constrained; extrapolating $v_{\text{esc}}(R)$ to large $R$ requires a potential model.

Here, we use the Kenyon et al. (2008) potential model that is tied to observed Milky Way mass measurements. To establish $v_{\text{esc}}(R)$ in this model, we drop a test particle at rest from $R = 500$ kpc (i.e., half-way to M31) and calculate its trajectory down to $R = 0$ kpc. The Kenyon et al. (2008) model predicts $v_{\text{esc}} = 585$ km s$^{-1}$ at $R = 8$ kpc in this definition of escape velocity, in good agreement with the Smith et al. (2007) observation. We fit a low-order polynomial to the calculated velocity as a function of distance and find

$$v_{\text{esc}}(R) = -2.39 \times 10^{-4}R^3 + 0.0588R^2 - 6.62R + Z \text{ km s}^{-1},$$

(3)

where $Z = 619$ km s$^{-1}$, valid for $15 < R < 100$ kpc.

To avoid imposing an arbitrary mass on our velocity dispersion measurement, however, we re-normalize Equation (3) to the observed envelope of negative velocity stars in our sample. Figure 6 shows the $v_{\text{esc}}(R)$ relation that we use, with $Z = 500$ km s$^{-1}$ (Equation (3)). Our assumption in changing $Z$ to 500 km s$^{-1}$ is that the velocity distribution of halo stars extends up to the escape velocity, and that the most negative velocity stars—the stars falling in from the largest distances—provide the most robust measure of escape velocity in our data set. Perets et al. (2009) discuss this further in the context of HVSs. We test the effects of our choice of $v_{\text{esc}}(R)$ by using a non-parametric approach to calculate velocity dispersion in the next section. In this section, we calculate the velocity dispersion profile by using the shape of the $v_{\text{esc}}(R)$ relation to provide a physically motivated means of clipping velocity outliers.

We plot the resulting velocity dispersion of stars with velocities less than $v_{\text{esc}}(R)$ for $Z = 500$ km s$^{-1}$ in the lower panel of Figure 6. Our Monte Carlo approach allows outliers that might otherwise be clipped to contribute a weight appropriate to their measurement uncertainties. A linear least-squares fit to the velocity dispersion profile finds a declining velocity dispersion,

$$\sigma_v = (-0.30 \pm 0.10)R + (120 \pm 4.6) \text{ km s}^{-1},$$

(4)

valid over $15 < R < 75$ kpc. A higher-order fit does not significantly improve the residuals. The linear fit has a standard deviation of $4.8$ km s$^{-1}$ and a reduced $\chi^2$ of 0.7. A fixed velocity dispersion, by comparison, has a standard deviation of $7.6$ km s$^{-1}$ and a reduced $\chi^2$ of 1.5, poorer than the linear fit but not statistically inconsistent.

3.3. Velocity Dispersion: Caustic Method

A non-parametric approach to determining the velocity dispersion profile leads to robust results based on fewer a priori
indicating the escape velocity from the system. The amplitude from the cluster center. In this plane, cluster members distribute

\[
A(r) = \int_0^R \mathcal{A}(r) \varphi(r) dr / \int_0^R \varphi(r) dr
\]

(5)
is the mean caustic amplitude within \( R \), \( \varphi(r) = \int f_g(r,v) dv \). \( R \) is not a free parameter in the standard application of the technique, but here we chose \( R = 30 \) kpc. Our results are totally insensitive to this parameter: varying \( R \) in the range 20–100 kpc varies the final number of the halo members by at most five and does not change the velocity dispersion profile.

We use an iterative approach to estimate the velocity dispersion profile. First, we compute the velocity dispersion of the total sample and locate the caustics that enable some interloper removal. We then compute a new velocity dispersion with the member stars, locate new caustics, and remove further interlopers. We proceed until no star is identified as an interloper. This procedure requires only four steps and on average yields 838 (of 910) final halo members and an overall velocity dispersion of 99 km s\(^{-1}\). The final set of caustics is drawn with the solid line in the upper panel of Figure 6.

The open triangles in the lower panel of Figure 6 show the caustic velocity dispersion profile. It is visually apparent that the caustic technique measures the velocity dispersion from the well-sampled core of the velocity distribution. This approach results in a reliable velocity dispersion profile, but yields a velocity dispersion that is systematically 10% smaller than found by our parametric \( \sigma_{esc}(R) \) method. We conclude that clipping velocity outliers with the caustic technique changes the observed amplitude, but not the observed slope, of the velocity dispersion profile.

A linear least-squares fit to the caustic velocity dispersion profile finds a declining velocity dispersion,

\[
\sigma_c = (-0.45 \pm 0.16) R + (110 \pm 6.0) \text{ km s}^{-1},
\]

valid over 16 < \( R < 64 \) kpc. The linear fit has a standard deviation of 4.8 km s\(^{-1}\) and a reduced \( \chi^2 \) of 1.0. A fixed velocity dispersion, by comparison, has a standard deviation of 7.9 km s\(^{-1}\) and a reduced \( \chi^2 \) of 2.8. In this case, a constant velocity dispersion is a significantly poorer fit to the data.

3.4. Possible Systematics

There are at least two contaminants that may systematically affect our velocity dispersion profile: binary stars, which increase the velocity dispersion, and disk stars (i.e., white dwarfs), which decrease the velocity dispersion. We investigate how these contaminants may alter the observed velocity dispersion profile.

Binary stars are unlikely to change the velocity dispersion profile. Both BHB stars and 1.5 \( M_\odot \) blue stragglers have stellar radii around 2.5 \( R_\odot \). Equal mass pairs of such stars must have semimajor axes of at least 6.5 \( R_\odot \) to avoid Roche lobe overflow. Thus, the most compact possible binary system has velocity semiamplitude of 100 km s\(^{-1}\). Assuming that half of the targets are binaries with a lognormal distribution of semimajor axes, we expect 30 binaries in our data set with \( v \sin i > 50 \) km s\(^{-1}\). This estimate is generous given that BHB stars have recently evolved through the red giant phase and are thus unlikely to have close companions. In any case, binaries will be observed at a random orbital phase and binned with 70–200 other stars to compute a velocity dispersion. We propagate our simulated distribution of \( v \sin i \)'s through our Monte Carlo catalog and find a negligible change in the velocity dispersion profile; the uncertainty in the velocity dispersion slope remains 30%.

Disk stars pose a greater threat to the velocity dispersion profile. Disk stars have a systematically lower velocity dispersion than halo stars and may also have a non-zero mean velocity because of the longitude dependence of the Sun’s circular velocity correction. The SDSS imaging survey from which we draw our candidates does not uniformly survey the sky across all longitudes.

Our greatest concern is white dwarfs, which are intrinsically faint and overwhelmingly appear at faint magnitudes in our survey. Inserting white dwarfs into our halo sample thus reduces the velocity dispersion observed at large distances. Observationally, 15% of our survey targets are white dwarfs, mostly found at low latitudes. If we insert a 1% white dwarf contamination into our Monte Carlo catalog, the resulting velocity dispersion profile steepens by 10%. Fortunately, white dwarfs are readily identified by their broad Balmer lines (see Kilic et al. 2007a). Visual inspection of our spectra reveals no white dwarf contaminants.

Binaries also have observational constraints. We obtained repeat observations for every star with \( |v_r| > 300 \) km s\(^{-1}\) and found only one star, a star near –300 km s\(^{-1}\), to exhibit radial velocity variation. We thus excluded this star from the halo sample. We conclude that binaries and white dwarfs are unlikely to significantly influence the velocity dispersion profile measured from our halo star sample.
3.5. Comparison with Previous Results

There are few measurements of the Milky Way velocity dispersion profile at large $R$. The most comparable measurements are Battaglia et al. (2005) and Xue et al. (2008). Battaglia et al. (2005) measure the velocity dispersion profile based on a sample of 9 satellite galaxies, 44 globular clusters, 58 red giants, and 130 BHB stars that span $10 < R < 140$ kpc. Xue et al. (2008) measure the velocity dispersion profile based on a sample of 2401 BHB stars that span $5 < R < 60$ kpc. With the exception of a handful of shared BHB stars, the samples are independent of one another.

Figure 7 compares the velocity dispersion profile and radial number distribution of our sample with those of Battaglia et al. (2005) and Xue et al. (2008). Beyond $R > 50$ kpc, our sample contains a factor of 8 more stars than Battaglia et al. (2005) and a factor of 2 more stars than Xue et al. (2008). Remarkably, the velocity dispersions measured by the three samples are consistent at the 1.5σ level. The three samples also observe a statistically similar decline in velocity dispersion with distance. The major difference between the samples is the significance of the observed decline in velocity dispersion with distance.

A linear least-squares fit to the Xue et al. (2008) data gives a $-0.15 \pm 0.14$ km s$^{-1}$ kpc$^{-1}$ decline in velocity dispersion over $10 < R < 60$ kpc. The linear fit has a standard deviation of 6.3 km s$^{-1}$ and a reduced $\chi^2$ of 1.5. A fixed velocity dispersion has a very similar standard deviation of 6.4 km s$^{-1}$ and reduced $\chi^2$ of 1.9. Thus, the Xue et al. (2008) measurements cannot formally discriminate between a constant velocity dispersion and a declining velocity dispersion.

The Battaglia et al. (2005) data, on the other hand, exhibit a steeper $-0.58 \pm 0.11$ km s$^{-1}$ kpc$^{-1}$ decline in velocity dispersion over $10 < R < 100$ kpc. We exclude their last bin because it contains only three objects. The linear fit has a standard deviation of 8.6 km s$^{-1}$ and a reduced $\chi^2$ of 0.85.

The weighted average of all the samples yields a $-0.38 \pm 0.12$ km s$^{-1}$ kpc$^{-1}$ decline in velocity dispersion over $10 < R < 100$ kpc. We obtain the same result if we average only our own two velocity dispersion measurements. The Milky Way velocity dispersion profile is not linear, of course, but three independent sets of observations are in statistical agreement: the Milky Way radial velocity dispersion drops from $\sigma \simeq 110$ km s$^{-1}$ at $R = 15$ kpc to $\sigma \simeq 85$ km s$^{-1}$ at $R = 80$ kpc.

4. CONCLUSIONS

The mass and mass distribution of the Milky Way are fundamental parameters because they link directly to theoretical models. We use a spectroscopic sample of 910 halo stars derived from our HVS survey to measure the velocity dispersion profile of the Milky Way. The stars are 74% BHB stars and 26% blue stragglers. We estimate luminosities using stellar evolution tracks for metal-poor main-sequence stars and BHB stars. Because of the non-Gaussian distribution of luminosity estimates, we use a Monte Carlo approach to calculate velocity dispersion and its uncertainty.

We calculate the velocity dispersion profile in two ways: a parametric method based on a $v_{esc}(R)$ model and a non-parametric method based on the caustic technique originally developed to measure galaxy cluster mass profiles. Comparing the two methods provides a measure of the systematic uncertainty arising from the clipping of outliers in velocity. The velocity dispersion from the caustic method is 10% smaller than the $v_{esc}(R)$ method, but both methods identify a similar decline in velocity dispersion with distance: $-0.38 \pm 0.12$ km s$^{-1}$ kpc$^{-1}$, valid for $15 < R < 75$ kpc.

Our sample contains a factor of 8 more stars than Battaglia et al. (2005) and a factor of 2 more stars than Xue et al. (2008) at $R > 50$ kpc. The velocity dispersion profiles observed by these independent data sets are consistent at the 1.5σ level, and have an average velocity dispersion slope identical to our result. Remarkably, no matter what tracers are used, observers find the same halo velocity dispersion profile.

The velocity dispersion profile is a basis for measuring the total mass and mass distribution of the Milky Way halo. A companion paper by O. Gnedin et al. (2010, in preparation) presents the theoretical calculations that turn the observed velocity dispersion profile into a mass determination of the Milky Way.

For further progress in measuring the Milky Way velocity dispersion profile, it is essential to identify tracers at distances $R > 50$ kpc. It is difficult to find $R > 50$ kpc tracers because of the steep decline in the density of the stellar halo. It is also very difficult for proper-motion surveys to measure tracers at $R > 50$ kpc distances. Ongoing spectroscopic radial velocity surveys, such as the SDSS-3 survey and our own HVS survey, promise to better trace the Milky Way in coming years.

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Facilities: MMT (Blue Channel Spectrograph)
APPENDIX

DATA TABLE

Table 1 presents the 910 stars used here. We provide the observed positions, magnitudes, and velocities plus our derived luminosities, distances, and BHB likelihood. The table columns are (1) R.A. (J2000), (2) decl. (J2000), (3) dereddened SDSS $g_0$ magnitude, (4) magnitude error, (5) dereddened SDSS $(u-g)_0$ color, (6) $(u-g)_0$ error, (7) dereddened SDSS $(g-r)_0$ color, (8) $(g-r)_0$ error, (9) heliocentric radial velocity $v_{helio}$, (10) velocity error, (11) Galactic longitude $l$, (12) Galactic latitude $b$, (13) Galactic rest-frame velocity $v_{helio}$, as defined in Equation (1), (14) BHB absolute magnitude $M_{BHB}$ derived from Dotter et al. (2008) for [Fe/H] = −1.9, (15) magnitude error, (16) BHB Galactocentric distance $R_{BHB}$, (17) blue straggler absolute magnitude $M_{BS}$ derived from Girardi et al. (2004) for [Fe/H] = −1.9, (18) magnitude error, (19) blue straggler Galactocentric distance $R_{BS}$, and (20) the star’s likelihood of being BHB, $0 < f_{BHB} < 1$, based on stellar colors and spectra (the full version of Table 1 is available in the online journal).

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