A COUPLED ANALYSIS OF ATMOSPHERIC MASS LOSS AND TIDAL EVOLUTION IN XUV IRRADIATED EXOPLANETS: THE TRAPPIST-1 CASE STUDY

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ABSTRACT

Exoplanets residing close to their stars can experience evolution of both their physical structures and their orbits due to the influence of their host stars. In this work, we present a coupled analysis of dynamical tidal dissipation and atmospheric mass loss for exoplanets in XUV irradiated environments. As our primary application, we use this model to study the TRAPPIST-1 system, and place constraints on the interior structure and orbital evolution of the planets. We start by reporting on a UV continuum flux measurement (centered around \(\sim 1900\) Angstroms) for the star TRAPPIST-1, based on 300 ks of Neil Gehrels Swift Observatory data, and which enables an estimate of the XUV-driven thermal escape arising from XUV photo-dissociation for each planet. We find that the X-ray flaring luminosity, measured from our X-ray detections, of TRAPPIST-1 is \(5.6 \times 10^{-4} L_\star\), while the full flux including non-flaring periods is \(6.1 \times 10^{-5} L_\star\), when \(L_\star\) is TRAPPIST-1’s bolometric luminosity. We then construct a model that includes both atmospheric mass-loss and tidal evolution, and requires the planets to attain their present-day orbital elements during this coupled evolution. We use this model to constrain the ratio \(Q' = 3Q/2k_2\) for each planet. Finally, we use additional numerical models implemented with the Virtual Planet Simulator VPLanet to study ocean retention for these planets using our derived system parameters.

Subject headings: stars: individual (TRAPPIST-1)

1. INTRODUCTION

TRAPPIST-1 provides a rare opportunity to study multi-planet systems around stars at the low-mass edge of the main sequence. The star TRAPPIST-1 is a M dwarf that hosts seven transiting planets in a highly compact configuration. The discovery of the first three planets was reported in Gillon et al. (2016), followed by the subsequent detection of four more planets (Gillon et al. 2017). Since TRAPPIST-1 has a V-band magnitude of 18.8 (Winters et al. 2015), mass determination for the planets is difficult with radial velocity methods. Instead, mass estimates and constraints on other orbital parameters have been constructed using transit timing variations (TTVs) (e.g., Gillon et al. 2017; Grimm et al. 2018). One major goal in the dynamical studies of planetary bodies is to understand their interior and exterior structures, which provide insights regarding how they formed. Planetary interior structures are often characterized in terms of a concentration parameter \(k_2\) (the Love number) and their tidal dissipation susceptibilities \(Q\) (the tidal quality factor). The exterior structures of the planets, in contrast, are characterized by the chemical abundances in their atmospheres, which are influenced by atmospheric mass loss rates.

In recent years, the increasing quantity of observational data has allowed some constraints to be placed on the \(k_2\) and \(Q\) values of exoplanets (e.g., Jackson et al. 2008; Batygin et al. 2009; Kramm et al. 2012; Becker & Batygin 2013; Buhler et al. 2016; Csizmadia et al. 2019). Simultaneously, as the planets evolve dynamically, their atmospheres also experience mass loss over time due to the XUV irradiation provided by the host star. The XUV radiation that allows atmospheric mass loss includes both X-ray photons (with wavelengths between \(\sim 1\) and 100 Angstroms) and EUV photons (with wavelengths between 100 and 912 Angstroms). The specific mechanism that drives mass loss, and the structure of flows driven by the XUV flux, depends on the planetary properties and stellar luminosity levels (Owen & Jackson 2012). Nonetheless, the general process involves the XUV radiation ionizing hydrogen atoms and heating the gas in the upper planetary atmosphere, and the X-ray radiation penetrating farther and driving an outward flow from deeper in the atmosphere. The net effect of both of these types of radiation flux is to break down the more massive molecules into ionized forms in the upper atmosphere; these components are liberated more easily and lead to atmospheric mass loss (Vidal-Madjar et al. 2003).
In this work, we model the planetary and stellar tidal dissipation and planetary atmospheric mass loss for exoplanets experiencing XUV irradiation. We then use this model to study the TRAPPIST-1 system, and place constraints on the interior structure and orbital evolution of the planets. Specifically, we constrain the allowed values of the \( Q' \) ratio for each of the planets, with the four inner planets producing independent lower limits on their planetary \( Q' \) ratios.

This paper is organized as follows. In Section 2, we describe the Neil Gehrels Swift Observatory (Swift) data set and derive fundamental parameters for the host star TRAPPIST-1 and its planets. In Section 3.1 we discuss the theoretical insights that can be gained by considering a simultaneous analysis of both mass loss and planetary migration in these systems. Section 3.2 considers how the measured and estimated parameters (the XUV flux and planetary \( Q' \) ratios) affect ocean retention for each planet in the system. In Section 4 we consider the implications of our results on the radiation environments and likely dynamical properties of the TRAPPIST-1 planets. Finally, the paper ends in Section 5 with a summary of our results and suggestions for future lines of inquiry.

2. DATA AND DERIVED PARAMETERS

2.1. SWIFT Data

Our data set consists of 34 epochs of observations of TRAPPIST-1 using the Swift Ultraviolet/Optical Telescope (UVOT), for a total of \(~300\) ks on target. The observations were taken between September 14, 2017 and July 8, 2018 using the uvw2 filter, which has a central wavelength of 1928 Angstroms and a full width at half maximum of 657 Angstroms (Poole et al. 2008). TRAPPIST-1 was also observed with XRT in photon-counting mode simultaneously with the UVOT measurements, and recorded photons with energies between 0.2 and 10 keV (Burrows et al. 2005). These two data sources allow a characterization of the UV and X-ray behavior of TRAPPIST-1 in both flaring and quiescent states. We describe the ways in which the data was processed in this section.

2.1.1. SWIFT UVOT Dataset

This filter provides a measurement of the UV continuum to the redder side of the Lyman-\( \alpha \) feature, which is generally used as a proxy of the continuum flux in the UV (Bourrier et al. 2017).

The UVOT data were obtained in event (photon-counting) mode and reprocessed using the standard pipeline. We then used the XSELECT program\(^1\) to remove periods of background flaring (defined as departures \( \sigma \) above the mean for each exposure; this is typically minimal for SWIFT and resulted in very few removals) and to measure the flux through aperture photometry in each observation.

Source regions are defined using Source Extractor (Bertin & Arnouts 1996) using identical extraction radii (5 arcseconds) and background regions for each exposures. The background region is used as a local background to estimate the background level in the detection cell. The aperture photometry measurements are presented in Table 1. We note that this procedure, which gives us more control over the good time intervals, is consistent with aperture photometry on the standard SWIFT image products. The light curve from these measurements is shown in Figure 1.

We note that the SWIFT uvw2 filter has a known red transmission leak (non-zero transmission in the optical band). For red sources, optical light can significantly contaminate the uvw2 band. We therefore estimated the contribution from the Johnson \( U \) and \( V \) band fluxes for TRAPPIST-1 (assuming a quiescent, average value over the SWIFT baseline), as the red leak is negligible beyond \( V \). We find that, at most, the contribution is about 0.001 counts per second, which is consistent with the statistical uncertainty.

| Obs. ID | Observation Start (JD-2400000.5) | Observation End (JD-2400000.5) | Counts / sec |
|---------|---------------------------------|-------------------------------|-------------|
| 10283001 | 58010.35                        | 58010.77                      | < 0.020     |
| 10283002 | 58095.98                        | 58096.98                      | < 0.022     |
| 10283003 | 58097.65                        | 58097.72                      | < 0.020     |
| 10283004 | 58103.41                        | 58103.81                      | < 0.018     |
| 10283005 | 58105.00                        | 58105.01                      | < 0.023     |
| 10283006 | 58113.71                        | 58113.99                      | < 0.023     |
| 10283007 | 58114.70                        | 58114.85                      | < 0.015     |
| 10283008 | 58117.96                        | 58118.31                      | < 0.012     |
| 10283009 | 58124.93                        | 58125.00                      | < 0.024     |
| 10283010 | 58126.32                        | 58126.41                      | < 0.020     |
| 10283011 | 58131.50                        | 58131.84                      | < 0.021     |
| 10283012 | 58133.17                        | 58133.30                      | < 0.026     |
| 10283013 | 58136.64                        | 58136.96                      | < 0.041     |
| 10283014 | 58236.92                        | 58237.00                      | < 0.024     |
| 10283015 | 58237.51                        | 58237.92                      | < 0.021     |
| 10283016 | 58243.30                        | 58243.56                      | < 0.054     |
| 10283017 | 58244.30                        | 58244.31                      | < 0.037     |
| 10283018 | 58250.93                        | 58251.00                      | < 0.030     |
| 10283019 | 58251.52                        | 58251.81                      | < 0.028     |
| 10283020 | 58257.90                        | 58257.99                      | < 0.027     |
| 10283021 | 58258.71                        | 58258.72                      | < 0.027     |
| 10283022 | 58264.81                        | 58265.63                      | 0.024 ± 0.005 |
| 10283023 | 58271.52                        | 58271.87                      | < 0.015     |
| 10283024 | 58278.02                        | 58278.77                      | < 0.013     |
| 10283025 | 58279.75                        | 58279.77                      | < 0.043     |
| 10283026 | 58285.60                        | 58286.00                      | < 0.018     |
| 10283027 | 58286.14                        | 58286.81                      | < 0.017     |
| 10283028 | 58287.32                        | 58287.32                      | < 0.033     |
| 10283029 | 58293.32                        | 58294.05                      | < 0.026     |
| 10283030 | 58296.42                        | 58296.97                      | < 0.019     |
| 10283031 | 58297.76                        | 58297.89                      | < 0.030     |
| 10283032 | 58298.76                        | 58299.96                      | < 0.026     |
| 10283034 | 58305.78                        | 58307.00                      | < 0.019     |
| 10283035 | 58307.05                        | 58307.92                      | < 0.019     |

All 58010.35 58307.92 0.0072 ± 0.0012

1 https://heasarc.gsfc.nasa.gov/ftools/xselect/
2.1.2. SWIFT XRT Dataset

In Figure 2, we present the detected photons as a light curve. The data was collected in XRT’s photon-counting mode. The light curve was produced by using a source extraction region centered at the sky position of TRAPPIST-1 and with a aperture radius of ≈45 arc-seconds, and a nearby background region of ≈ 88 arc-seconds. After detected photons in the source and background regions were recorded, the final light curve was produced using the XSELECT program, by binning the source and background light-curve to 5000 second bins and constructing the final corrected light-curve by subtracting the background off the source light-curve using XSELECT tool LCMATH.

The final result is plotted in Figure 2 and two colors of points are plotted: in red, bins when the source was detected, and in grey, bins where was not. The detections correspond to quiescent periods or just periods where the background was too high to detect the flaring source.

The light-curve describes the flux level over time, but to find an averaged flux level, we do not fit the light-curve itself; instead, we stack the entire 300 ks of data and extract the flux from that. Excluding the flaring times and stacking all observations of periods of time corresponding to non-detections within each 5000 s bin (time periods plotted as grey upper limits), we find a baseline quiescent flux of 0.00026 counts/sec. Including only the detections (time periods plotted as red points), we find a detected flux of 0.0024 counts/sec. Using a stacked image of all 300 ks of data, we find an average flux of 0.0012 counts/sec. These values are summarized in Table 2. Importantly, the background is not large enough to account for the non-detections for our derived value of flaring and quiescent flux.

2.2. Derived Parameters

From our light curve, we can derive several parameters describing the high-energy radiation environment of the system. As TRAPPIST-1 hosts at least seven planets whose habitability status and long-term atmospheric evolution depends tightly on their XUV insolation environments (O’Malley-James & Kaltenegger 2017), better constraints on these parameters allow better modeling of the evolution and history of the system.

2.2.1. UV Flux

Due to the large number of upper limits and low-significance detections, we measure the flux by utilizing a stacked image of the 300 ks of observations, centered on the sky position of TRAPPIST-1. From the stacked image, we find a 5σ detection of TRAPPIST-1, corresponding to a UVOT uvw2 count rate of of 0.0072 ± 0.0012 CPS (counts/sec). This count rate can be converted to a flux for a M-dwarf using the conversion rate given in Table 2 of Brown et al. (2016), resulting in a measure of the flux at Earth in the UV of 8.4 \( \times 10^{-15} \text{erg/cm}^2\text{s} \) (see Table 2 in the Swift uvw2 waveband around ∼ 1900 Angstroms).

2.2.2. X-ray Flux

The X-ray light curve has a large number of non-detections, and as such we also measure the X-ray flux by utilizing a stacked image of all photons received. From the stacked image, we find a background-corrected detection of TRAPPIST-1 with an XRT count rate of of 0.00042 ± 0.00005 CPS (counts/sec). The values for the count rates during detections and non-detections are also given in Table 2. This count rate can be converted to a flux for a M-dwarf using the two-temperature model from Wheatley et al. (2017). We do this by using a single conversion factor between Swift count rate and flux in erg/s/cm². This count rate was computed using XSPEC to recreate the model from Wheatley et al. (2017), and then using the Swift gain scale and effective area of the telescope (which come from the redistribution matrix file and appropriate ancillary response files for Swift). In this case, we find that 1 count/s corresponds to 2.67e-11 erg/s/cm² for the Swift parameters and energy bandpass.
2.3. UV Flaring Activity

A major goal of collecting a large quantity of Swift UV data on TRAPPIST-1 was to study the star’s flaring over time. Using the stacked image’s derived flux as the baseline value, we find one event where the instantaneous measured flux value exceeds the baseline by more than $\sim 3\sigma$. This occurs during observation ID 10283022, a roughly 19 ks observation taken starting on 2018-05-26 (see Table 1). All other observations yield either upper limits on the flux or measures consistent with the average flux level. The integrated flux level across all our observations (and the upper limit on flux from roughly a quarter of our non-detections) is much lower than this solid detection. Due to its significant observational baseline, our integrated 300 ks image is likely a good measure of the average UV flux emitted by the star, and we proceed with this averaged value in subsequent analysis in this paper.

2.3.1. EUV and XUV Flux

EUV (100 - 900 Angstroms) observations of stars in general are made difficult by two factors: first, EUV flux is absorbed by the ISM mainly around 400 - 900 Angstroms; second, the Earth’s geocoronal hydrogen is problematic when observing in the EUV. As such, the EUV flux (the wavelength needed for studies of atmospheric mass loss, among other analyses) cannot generally be directly measured.

However, the EUV flux can be extrapolated from wavebands where observations can be made using empirical scaling relations (Sanz-Forcada et al. 2011; Linsky et al. 2014; Sanz-Forcada et al. 2014; King et al. 2018). Since the sum of the EUV flux and X-ray flux controls the rate at which mass is lost from planetary atmospheres, in this work we use our direct measure of the X-ray flux to derive extrapolated values for the EUV flux. Our direct measure of the Swift UV flux (taken in a waveband centered near 2000 Angstroms) will ideally be useful for future photochemistry models (see Ranjan et al. 2017; Chen et al. [2019]) but is not directly used in the XUV models that follow in this paper.

From Sanz-Forcada et al. (2011), we have the empirically-derived mapping between EUV and X-ray luminosities:

$$\log L_{\text{EUV}} = (4.80 \pm 1.99) + (0.860 \pm 0.073) \log L_{\text{X}},$$

where this scaling relation was derived using GALEX data. We also caution that the samples used to empirically derive Equation 1 included very few M-dwarfs and only a single late-type M-dwarf, so this extrapolation is a significant source of uncertainty in our analysis (as are many empirical scaling relations; Drake et al. [2019]).

Using Equation 1, we convert the x-ray flux computed in Section 2.2.2 to a EUV flux. The resultant final value of the combined XUV flux and the intermediate steps are presented in Table 2.

### Table 2: EUV and XUV Fluxes

| Observation ID | EUV Flux (erg s$^{-1}$ cm$^{-2}$) | XUV Flux (erg s$^{-1}$ cm$^{-2}$) |
|---------------|---------------------------------|----------------------------------|
| 10283022      | $1.1 \pm 0.13 \times 10^{-14}$   | $2.6 \times 10^{-14}$            |
| 10278022      | $4.4 \times 10^{-15}$           | $1.2 \times 10^{-14}$            |
| 10278023      | $7.2 \times 10^{-15}$           | $1.4 \times 10^{-14}$            |
| 10283023      | $9.6 \times 10^{-15}$           | $1.6 \times 10^{-14}$            |

2.4. Comparison with Previous Work

Wheatley et al. (2017) found that this star is a strong coronal X-ray source, with an X-ray flux of $2 \times 10^{-14}$ erg s$^{-1}$ cm$^{-2}$.

Peacock et al. (2019) created model spectra to derive model fluxes in the EUV, which cannot be observed directly, and found results varying between $1.32 - 17.4 \times 10^{-14}$ erg s$^{-1}$ cm$^{-2}$, depending on the model used. From scaling relationships, previous work obtained values ranging between $0.7 - 5.8 \times 10^{-14}$ erg s$^{-1}$ cm$^{-2}$ (Bourrier et al. 2017) [Wheatley et al. 2017]. Our observations imply a EUV flux at Earth of $2.6 \times 10^{-14}$ erg s$^{-1}$ cm$^{-2}$, which is roughly consistent with Model 1A of Peacock et al. (2019). Model 1A was constructed...
by calibrating to the the Lyα observations for this star, while the other models were matched to GALEX fluxes for M8 field stars. Our results are also consistent with the empirical model’s prediction from Berger et al. (2010) (see Figure 3 of that paper, which finds that for an M8 dwarf, log $L_X/L_{bol}$ falls between -4 and -3.5, while we find log $L_X/L_{bol} \approx -4$) for a star of this spectral type.

2.4.1. Planetary mass loss rates

Equation 1 of Bourrier et al. (2017b) computes the mass loss rate (see the original calculation in Watson et al. 1981 as well as Erkaev et al. 2007, Lopez et al. 2012, and Luger et al. 2015) to have the form:

$$m_p = \epsilon (r_{XUV}/r_p)^2 (3 F_{XUV}/4 G \rho K)$$

(2)

where $\epsilon$ is the heating efficiency (set to be equal to 0.1 in this work), $r_p$ is the true radius of the planet, $r_{XUV}$ is the effective planetary radius in the XUV waveband (which we assume is approximately equal to the true radius in this work, since the planet is rocky), $F_{XUV}$ is the XUV flux received by the planet, $G$ is the gravitational constant, and $K$ is a tidal enhancement factor (Erkaev et al. 2007), defined such that

$$K = 1 - \frac{3}{2} \frac{r_{XUV}}{r_{roche}} + \frac{1}{2} \frac{r_{XUV}}{r_{roche}}^3$$

(3)

where $r_{roche}$ is the planetary Roche Lobe (defined as $r_{roche} = (m_p/2M_*)^{1/3} a$). For planets at short orbital periods, $K$ describes the enhancement in escape potential for gas in the planetary atmosphere: the proximity to the star and large effect of stellar gravity means that gas must reach the Roche radius to escape the planet.

From Equation 2, we can compute the expected mass loss rates for each of the planets in the TRAPPIST-1 system at the current day. These values are given in Table 3.1. We note that although these rates are small at the current day, they are likely not constant over the age of the system. In the first 500 Myr of the system lifetime, the bolometric luminosity was much brighter (Baraffe et al. 2015) and thus the mass loss rates equivalently higher (barring shielding against photo-evaporation due to the disk while the gas disk was still present).

3. THEORETICAL IMPLICATIONS

There has been a significant amount of follow-up observations on the TRAPPIST-1 system, resulting in high-precision measurements of the planetary orbital parameters. The earliest analyses of the system, in which the planet discoveries were announced, reported only upper limits for eccentricities (Gillon et al. 2017), but recent work using a longer observational baseline finds the eccentricities of all planets are non-zero, to significance levels varying between 2σ and 10σ (Grimm et al. 2018).

TRAPPIST-1 b’s eccentricity being 2σ inconsistent with zero is particularly intriguing, since its extremely short current-day orbital period indicates that it will be susceptible to tidal decay of eccentricity and semi-major axis. Many papers (i.e Papaloizou et al. 2018) have conducted their analysis of the TRAPPIST-1 system by assuming null eccentricities for all planets, as such a configuration boosts dynamical stability and increases the timescale on which the system can be studied numerically without becoming destabilized. In this work, however, we consider the implication of the potential non-zero eccentricity on the tidal parameters of the planets, and discuss the impact these arguments have on our understanding of the planetary eccentricities.

3.1. Analytic Modeling of Tidal and Atmospheric Evolution

The rate of orbital radius change expected due to tides has two components: one due to the tides raised on the planet, and another due to the tides raised on the host star. This change may manifest as either a decay (i.e., Barnes et al. 2008, Silburt & Rein 2015) or an expansion of the orbits (as for the moon; Murray & Dermott 1999), depending on the specific tidal, spin, and orbital parameters of the involved bodies. In this section, we consider whether the currently observed planetary eccentricities in the TRAPPIST-1 system are likely to persist on timescales of order the age of the system by using TRAPPIST-1 b as the boundary condition. If TRAPPIST-1 b, the most susceptible planet to eccentricity damping, can maintain its eccentricity under the effects of both tidal evolution due to interactions with its host star and atmospheric mass loss due to stellar EUV insolation, then likely all planets can.

The magnitude of these effects can be estimated using the following expression from Goldreich (1963) (with expressions written in a functionally identical form to that used in Barnes et al. 2008):

$$ \frac{da}{dt} = \left( -\frac{63}{2} \frac{1}{Q' m_p} \sqrt{GM_5 R_p^5 \rho_e^2} + \frac{9}{2} \frac{Q}{Q_v} \sqrt{G/MR_s^5 m_p} \right) a^{-11/2},$$

(4)

where $Q' = 3Q/2k_2$ is three halves times the ratio of the effectiveness of a body’s rate of energy dissipation due to tidal distortions ($Q$) to the the love number ($k_2$, describing a body’s central concentration), $m_p$ denotes a planetary mass, $r_p$ denotes a planetary radius, $G$ is the gravitational constant, $M$ denotes the stellar mass, $R$ the stellar radius, $a$ denotes the planetary semi-major axis, $e$ the planetary eccentricity, and the term $\sigma = sign(2\Omega - 3n)$ (where $\Omega$ is the stellar spin rate and $n$ the planetary mean motion) describes the relative frequencies of the stellar rotational period and planetary orbital period. In Gillon et al. (2016), the TRAPPIST-1 rotation rate was estimated using ground-based data to the $P_{rot} = 1.40$ days, but follow-up work using data from the K2 spacecraft (Luger et al. 2017, Vida et al. 2017) provided an updated value of $P_{rot} = 3.33$ days, which we use in this analysis. This value of $P_{rot} = 3.33$ days (giving the star a rotational period situated in between the orbital periods of planets c and d) means that the sign term $\sigma$ in Equation 4 cannot be neglected, as different planets will be affected differently by tides raised on the star. We do note that as $Q_*$ is very large (in this work, we use $Q_* = 10^5$, while estimates for stars range between $10^4$ and $10^6$; Jackson et al. 2009), the second term of this equation will have a negligible effect compared to the first term, leading to tides raised on the planet rather than those raised on the star having the dominant effect in the orbital evolution of the planet.


A secondary paired equation can be written to describe the evolution of eccentricity over time (Goldreich 1966):

\[
d\epsilon/dt = \left(-\frac{63}{4} \frac{1}{Q' m_p} \sqrt{GM^3 r_p^5} + \frac{171}{16} \frac{\sigma}{Q' \sqrt{G M R^5 m_p}} \right) a^{-13/2},
\]

where the first term is due to tides raised on the planet and the second term is due to tides raised on the star. Combined with Equation 4, these two expressions describe the decay of a planet’s orbit, which will occur more quickly for planets which dissipate their stored energy very quickly (i.e., more rocky planets, or those with lower \(Q’\)).

All of the parameters in both of these equations can be measured from the TRAPPIST-1 light curve (radii directly, and masses via transit timing variations as in Grimm et al. (2018), and stellar parameters using the K2 data as in Luger et al. (2017) except for the \(Q’\) ratio, which describes the physical structure of the planet. Since the change in orbital elements scales roughly linearly with \(Q’\), slightly different interior structures can result in different timescales for the damping of orbital eccentricity.

Then, based on the currently measured orbital parameters and an estimate of the age of the system, the true value of the \(Q’\) ratio can be estimated on the basis of a dynamical analysis (as is commonly done for hot Jupiters, whose \(Q’\) values must allow them to survive through the age of the system until our current observations; Barker & Ogilvie 2009). In the case of TRAPPIST-1, the relatively short orbital periods, combined with the non-zero eccentricities (if confirmed), would yield strong indirect constraints on the planets’ internal structure.

There is an added complication on the observed dynamics due to the evaporating atmosphere. If the XUV flux is high enough that the planets are losing atmospheric mass, then our current-day estimates of the orbital decay might be overestimated (if only slightly, given that the computed mass loss rates are very slow). To fully encapsulate the tidal dynamics of this system, all the factors enumerated above must be considered, which we do by solving the evolution as a coupled set of differential equations, as follows.

To model the expected evolution of eccentricity and semi-major axis for TRAPPIST-1 b (for now, neglecting planet-planet interactions and treating the short-period TRAPPIST-1 b as the edge case where constraints will be most easily derived), we combine and solve the system of differential equations including the damping of semi-major axis and eccentricity due to tides, as well as the atmospheric loss rate computed in Section 2.

\[
\begin{align}
\frac{de}{dt} &= \left(-\frac{63}{4} \frac{1}{Q' m_p} \sqrt{GM^3 r_p^5} + \frac{171}{16} \frac{\sigma}{Q' \sqrt{G M R^5 m_p}} \right) a^{-13/2} \\
\frac{da}{dt} &= \left(-\frac{63}{4} \frac{1}{Q' m_p} \sqrt{GM^3 r_p^5} + \frac{171}{16} \frac{\sigma}{Q' \sqrt{G M R^5 m_p}} \right) a^{-13/2} \\
\frac{dm_p}{dt} &= \epsilon (r_{XUV}/r_p)^2 (3F_{XUV}/4GpK)
\end{align}
\]

where for now we assume \(F_{XUV}\) is constant over time (this is a good approximation when modeling evolution in M-dwarfs taking place when the star is more than 1 Gyr old; see the models of Baraffe et al. 2015). We note that for larger mass stars where the luminosity does change appreciably over the main sequence lifetime of the star, an additional coupled equation \(dL_\star/dt\) should be added to the system, where the stellar luminosity can be numerically modeled (using, for example, the models of Baraffe et al. 2015). Note that this was done in Luger & Barnes (2015); Luger et al. (2015); Lincowski et al. (2018).

To study the pre-main sequence behavior of these planets, this variable luminosity would need to be accounted for (see Section 3.2). We also assume that the TRAPPIST-1 planets, being similar in radius to the Earth, are terrestrial and will lose mass from their atmospheres, leading to the planetary \(Q’\) ratios being constant over the age of the system.
| Planet      | Period (days) | Radius (R$_\oplus$) | Mass (M$_\oplus$) | e  | XUV Flux (erg/cm$^2$/s) | Mass loss (gram/sec) | Mass loss (M$_\oplus$/Gyr) |
|------------|---------------|----------------------|-------------------|----|------------------------|----------------------|-----------------------------|
| TRAPPIST-1 b | 1.510876      | 1.121                | 1.017             | 0.00622 | 2905.128486             | 8.286578e+08         | 0.004376                     |
| TRAPPIST-1 c | 2.421807      | 1.095                | 1.156             | 0.00654 | 1564.865012             | 3.62544e+08          | 0.001913                     |
| TRAPPIST-1 d | 4.049959      | 0.784                | 0.297             | 0.00837 | 788.454573              | 2.607478e+08         | 0.001377                     |
| TRAPPIST-1 e | 6.099043      | 0.910                | 0.722             | 0.00510 | 456.452067              | 9.081431e+07         | 0.000480                     |
| TRAPPIST-1 f | 9.205585      | 1.046                | 0.934             | 0.01007 | 263.598217              | 6.583289e+07         | 0.000348                     |
| TRAPPIST-1 g | 12.354473     | 1.148                | 1.148             | 0.00208 | 178.116325              | 4.784535e+07         | 0.000253                     |
| TRAPPIST-1 h | 18.767953     | 0.773                | 0.331             | 0.00567 | 102.035492              | 2.902111e+07         | 0.000153                     |

Note. — Planetary parameters for the planets in the TRAPPIST-1 system. Orbital periods, planetary masses, radii, and eccentricities come from Grimm et al. (2018); errors from that paper are not reproduced in this table for brevity. The XUV flux incident on each planet and the resultant planetary atmospheric mass loss rates were derived in Section 2 of this work.

![Fig. 3.](image-url)  
**Fig. 3.** (Top panel) The fractional eccentricity dissipation over time for TRAPPIST-1 b, compared to the initial value at the time of disk dispersal $e_b(0)$. The evolution was computed by simultaneously solving the system given in Equation 6 with planetary semi-major axis fixed to its currently measured value. The forward evolution demonstrates the expected damping in eccentricity expected for this short-period planet by tidal parameter $Q'$. (Bottom panel) The percentage deviation between our model (which includes the mass loss, as planetary masses decrease at a rate given by Equation 2) and our model with the mass loss rate set to zero. When mass loss is accounted for, the time at which the planet circularizes occurs earlier than if it is ignored, and the difference is larger for larger values of $Q'$.

In Figure 3, we show the evolution of eccentricity of TRAPPIST-1 b over time under two major assumptions: first, the evolution is modeled starting at the time of disk dispersal, and we assume that the entire system of planets had attained roughly their current orbits at that time; second, we assume that the XUV luminosity of TRAPPIST-1 is constant over this time (and thus the evolution begins after the star has reached the main sequence). This analysis (and those that follow in this section) are intended to model the dynamical evolution of the system after the planets reach their final orbital periods, and determine how the tidal parameters $Q'$ of each of the planets affect that evolution. Figure 3 shows that the fractional eccentricity of TRAPPIST-1 b is damped fairly quickly (i.e., for a non-zero eccentricity to be maintained, another process must be at play).

Additionally, altering the initial parameters of this model will not change the exponential damping time scale, meaning that even if the eccentricities had been larger initially, they should have damped to zero by the
current day (that is, the fractional evolution shown in Figure 3 will hold for a range of starting planetary eccentricities, which does not necessitate that the planets had any particular values when the system was assembled.) The bottom panel of Figure 3 shows the percentage difference when the changing planetary masses are and are not considered; although the deviations between the two models are very small, the magnitude of the deviations are a function of planetary $Q'$, meaning that mass loss must be modeled when attempting to constrain $Q'$. In systems with higher mass loss rates, this effect would become even more important.

TRAPPIST-1 b resides at current day on a very short orbital period (1.5 days, which corresponds to a semi-major axis of $\sim 0.011$ AU). At the same time, the Grimm et al. (2018) measurement of the current-day eccentricity of TRAPPIST-1 b is $0.00622 \pm 0.00304$. Among the planets in the TRAPPIST-1 system, planet b (having a non-zero eccentricity and the shortest orbital period) will be the most susceptible to eccentricity damping due to interactions with its host star.

In Figure 4 we plot the evolution of eccentricity for each planet as it depends on the $Q'$ ratio chosen for that particular planet. The timescales upon which the eccentricity will be damped can be determined from Equation 8 and the chosen value of $Q'$.

In Figure 5 we plot the dependence of the final system eccentricity at various times as it depends on the planetary $k/Q$ ratio. We also plot for comparison the range of allowable $Q'$ derived in Papaloizou et al. (2018). In that work, authors derived the values of $Q'$ which allowed the planets to keep semi-major axis values close to their current resonant values over the course of the migration; their derived limit of $Q' > 1.2 \times 10^9 (t/5 \text{ Gyr})$ reduces to $Q' > 1.8 \times 10^3$ for system age $t = 7.6$ Gyr (Burgasser & Mamajek 2017). In this work, we plot the values of $Q'$ that allow the eccentricities to be observationally determined to be non-zero, disallowing constraints where the departure from zero eccentricity could not be measured with the precision of the current TTV fits of Grimm et al. (2018). This analysis presents a lower limit for $Q'$ for the inner four planets (constraints cannot be made for the outer three planets, as any $Q'$ allows the observed eccentricity values).

### 3.2. Numerical Modeling of Tidal and Atmospheric Evolution

In the previous section, we considered the evolution of the system using a simple model which can be easily computed and used in conjunction with Monte Carlo techniques to robustly explore the (in this case, $k/Q$) relevant parameter spaces in the system. In this section, we turn to numerical techniques to model how our derived value of the XUV luminosity of the host star TRAPPIST-1 affects the capabilities of its seven planets to maintain surface water, and how the $Q'$ ratio affects ocean retention.

We use the Virtual Planet Simulator VPlanet 2 (Barnes et al. 2019) to numerically consider the evolution of the TRAPPIST-1 system in the presence of tides and atmospheric mass loss, the same processes considered in the previous section. In addition to the processes described in the previous section, VPlanet can simultaneously model the stellar, orbital, rotational, and even climate evolution of the system over time (Barnes et al., 2019), and has been used to study magma oceans on the TRAPPIST-1 planets (Barth et al, in prep.). Here, we use VPlanet modules EqTide (which uses the same constant-phase-lag model used in the analytic modeling above) to model tidal evolution, but using the full set of equations rather than just those for $da/dt$ and $de/dt$; see Appendix E of Barnes et al. (2019) and AtmEsc (which computes the energy-limited and diffusion-limited atmospheric escape; see Appendix A of Barnes et al. 2019). Between these two modules, we are able to self-consistently model the oceanic, atmospheric and tidal evolution of the (decoupled) planets.

We use as input to VPlanet the saturated $L_{XUV}/L_*$ ratio. The ratio we computed in Section 2.2.1 is the present-day value of this ratio; however, this ratio is known to decrease once the star spins down and leaves the ‘saturated’ regime, after which $L_{XUV}/L_{bol}$ decays exponentially (Pizzolato et al. 2003) - note that this decay is of the ratio $L_{XUV}/L_{bol}$ and is separate from any global change in $L_{bol}$. In Fleming et al. (2019), the authors use the Wheatley et al. (2017) value of $L_{XUV}$ luminosity and find that TRAPPIST-1 is likely (at a ~40% probability) still in its saturated phase. The Wheatley et al. (2017) measurement is a factor of two larger than the value computed in this work. To find the saturated XUV ratio which corresponds to the present-day XUV ratio we measure in this work, we use the best-fit values from Fleming et al. (2019) of the saturation timescale $t_{sat} = 6.85$ Gyr, $\beta_{sat} = -1.16$ (when $\beta$ is an exponent controlling how $L_{XUV}$ decays after saturation ends; see Equation 1 of Fleming et al. 2019).

Using these best-fit values and our own present-day measurement of $L_{XUV} / L_* = (3.4 \pm 0.4) \times 10^{-4}$, we model the evolution of the star TRAPPIST-1 alone (no planets) and find that our value (combined with the best-fit model from Fleming et al. 2019) corresponds to a saturated $L_{XUV} / L_*$ ratio of $L_{XUV} / L_* = 3.7 \times 10^{-4}$. We use this value as the input to VPlanet, which combined with the aforementioned Fleming et al. 2019 parameters
Fractional Ocean Retention

For TRAPPIST-1’s system evolution. For this combination with 20 Earth oceans of water (as compared to Lincowski et al. 2018, in which authors the planets with 10 Earth oceans worth of surface water for the full N-body evolution of the planets. We begin equations describing the tidal and atmospheric evolution parameters (taken from Grimm et al. 2018). Also use as inputs the currently measured best-fit planet evolution of the surface water composition over the first VPLanet

\[ Q_t \]

\[ Q = 600 \]

Fig. 6. For the theoretically allowable value \( Q' = 600 \), the VPLanet evolution of the surface water composition over the first 5 Gyr of the TRAPPIST-1’s system evolution. For this combination of \( Q' \) and \( L_{XUV} / L_\odot \), substantial oceans could be retained on planets d and h, and non-zero oceans retained on e, f, and g, while b and c will have totally lost their oceans. Some UV-motivated estimates of the current-day habitable zone of the system suggest that liquid water should only exist on planets e and beyond (O’Malley-James & Kaltenegger 2017), while others (Barr et al. 2018) find that it may still retain an ocean, consistent with our results for \( t_{\text{act}} \) and \( \beta \) causes the VPlanet luminosity evolution to reproduce our observed value after 7.6 Gyr. We also use as inputs the currently measured best-fit planet parameters (taken from Grimm et al. 2018). VPlanet simultaneously solves the coupled ordinary differential equations describing the tidal and atmospheric evolution of the planets. We note that in this work, we do not solve for the full N-body evolution of the planets. We begin the planets with 10 Earth oceans worth of surface water (as compared to Lincowski et al. 2018, in which authors conducted a similar analysis of and started the planets with 20 Earth oceans of water).

Following Papaloizou et al. (2018), we set the \( Q' \) values to be the same for all seven planets in each integration. We find that varying the values of \( Q' \) (within our previously derived allowable range) does not result in appreciably different ocean loss rates; the results of this numerical evolution, presented in Figure 6, were initialized with a \( Q' = 600 \) for all planets. We note that with \( Q' \) values below our allowed range (for example, \( Q' = 60 \)) the outcome resolved by VPLanet is collision with the central star; 3.1 to be more feasible given the current day planetary eccentricities. We see that with our extrapolated value of the XUV flux, the three inner planets do not retain surface water, losing it instead during the first Gyr of TRAPPIST-1’s lifetime. We do note that ground water could potentially replenish lost surface water, and the above analysis does not consider this potential effect.

4. DISCUSSION

In this work, we report on a continuum UV flux measurement of TRAPPIST-1, based on 300 ks of Swift UVOT data collected over a baseline of approximately one year (during which we isolate one possible flaring event). The measured value, of \( (8.4 \pm 1.4) \times 10^{-15} \) erg/cm\(^2\)/sec in the Swift uvw2 waveband centered around \( \sim 1900 \) Angstroms, is consistent with previous estimates for the specific star TRAPPIST-1 (Wheatley et al. 2017). We also present an X-ray flux measured with Swift XRT data of \( (1.1 \pm 0.13) \times 10^{-14} \) erg/cm\(^2\)/sec, which corresponds to a lower \( L_{XUV} / L_\odot \) ratio than found in previous work (Wheatley et al. 2017). Our derived values for the current EUV and XUV luminosities for TRAPPIST-1 as a fraction of the total luminosity are \((2.3 \pm 0.3) \times 10^{-4}\) and \((3.4 \pm 0.4) \times 10^{-4}\), respectively.

4.1. Conclusions on Planetary Eccentricities

As illustrated in Figure 3, the timescale over which the exponential damping of eccentricities occurs depends on the ratio \( Q' = 3Q/2k_2 \) of the planet. The planetary eccentricities measured in Grimm et al. (2018) were found to be non-zero by a significant margin. Under the assumption that these reported values are valid, we can make the following statements regarding the planetary eccentricities. One of the following two options must hold:

- The planets (particularly the inner planet, b) have a significant envelope capable of storing energy (and hence a larger ratio \( Q' = 3Q/2k_2 \)).
- The planetary eccentricities have already been damped and the non-zero eccentricities measured in Grimm et al. (2018) are not physical, but rather a result of the limited amount of data available at the present time.

The first option is supported by the conclusions of Papaloizou et al. (2018) and also Brasser et al. (2019), who also find that the \( Q' \) values for the TRAPPIST-1 planets must be large in order for the resonant chain to persist.

The planetary eccentricities considered above arise due to planet-planet interactions. Our dynamical analysis does not include planet-planet coupling, although the resonant state of the system suggests that the planets are indeed coupled. We can see from the numerical simulations of Papaloizou et al. (2018) that the net eccentricity will damp over time. At the same time, eccentricities of the current magnitudes appear to cause the system to go unstable over relatively short (<1 Gyr) timescales (Tamayo et al. 2017).

4.2. Conclusions on Planetary Tidal Qualities

Assuming that the planetary eccentricities are physical, their current values allow us to draw constraints on the \( Q' \) parameter for each planet.

The age of the star is estimated to be 7.6 ± 2.2 Gyr (Burgasser & Mamajek 2017). Figure 5 illustrates how the constraints on \( Q' \) depend on the age of the system: For a system younger than 7.6 Gyr, we get a smaller (less strict) lower limit for the allowable \( Q' \) ratio, as the eccentricity would have needed to be maintained for a smaller amount of time.

For TRAPPIST-1 b, we get the strongest constraint: for a 7.6 Gyr system age, we find that \( Q'_b > 600 \). For a typical \( k_2 = 0.3 \), this result corresponds to \( Q_b > 120 \). For planets c, d, and e, the limits are less strict. In our own solar system, the terrestrial planets have \( Q \) values estimated to be \( Q < 190 \) for Mercury, \( Q < 17 \) for Venus, \( Q \approx 12 \) for Earth, and \( Q < 26 \) for Mars (Goldreich & Soter 1966). In this context, our limit for TRAPPIST-1
b suggests a planet with Mercury-like dynamical properties and reactions to tidal deformation rather than one with properties more similar to Earth or Mars. The constraints on planets c, d, and e do not exclude Earth-like dynamical properties such as concentration and tidal dissipation susceptibilities. Papaloizou et al. (2018) find that in order for the resonances to persist on Gyr timescales while the planets migrate, the composite parameter $3Q/(2k_2)$ must be greater than $10^2 - 10^3$. This work uses separate considerations—allowing the measured eccentricities to persist (which does not depend on migration timescales). Nonetheless, we find that the limit for TRAPPIST-1 b is similar to that found in Papaloizou et al. (2018), where Figure 3 provides a direct comparison. On the other hand, our limits for the outer planets (c, d, and e) are similar to that found in Papaloizou et al. (2018), where Figure 3 provides a direct comparison. On the other hand, our limits for the outer planets (c, d, and e) are significantly less stringent. Moreover, our constraints are agnostic regarding the assembly mechanism of the system, relying only on the existence of eccentricity damping after the disk has dissipated.

5. SUMMARY

This paper develops a combined analytical treatment of the tidal evolution and XUV-driven atmospheric mass loss for close-in exoplanets, and applies it to the benchmark extrasolar planetary system TRAPPIST-1. We first estimate the average UV flux level of the TRAPPIST-1 star to be $8.4 \times 10^{-15}$ erg cm$^{-2}$ s$^{-1}$ (observed at Earth). Then, we measure the Swift X-ray flux of TRAPPIST-1, which corresponds to an extrapolated $Q$ and estimate their ranges of allowed $Q = 3Q/(2k_2)$ ratios, under the assumption that the currently measured orbital eccentricities from Grimm et al. (2018) are correct. For the outer three planets, no meaningful constraints can be made, and we cannot exclude Earth-like tidal $Q$ values for planets c, d, and e. For TRAPPIST-1 b, we find a lower limit of $Q > 600$, a limit larger that the $Q'$ values of our own solar system’s terrestrial planets. Further, our VPLanet analysis demonstrates that our measured UV and X-ray luminosities suggest that the third planet, TRAPPIST-1 d, may retain a surface ocean. The analytical method developed in this paper can be extended to planets with higher mass loss rates in order to study their coupled atmospheric and orbital evolution.

This project used the following software: pandas (McKinney 2010), IPython (Pérez & Granger 2007), matplotlib (Hunter 2007), scipy (Jones et al. 2001), numpy (Oliphant 2006), Jupyter (Kluyver et al. 2016), vplanet (Barnes et al. 2019), ds9 (Joye & Mandel 2003). Code, data, and supplemental figures related to this work can be found at https://github.com/jxcbecker/trappist1.

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