The upper bound of packet transmission-capacity in local static routing

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We propose a universal analysis for static routings on networks and describe the congestion characteristics by the theory. The relation between average transmission time and transmission capacity is described by inequality $T_i R_{c0} \leq 1$. For large scale sparse networks, the non-trivial upper bond of transmission capacity $R_{c0}$ is limited by $R_{c0} \leq 1/k > 1/k$ in some approximate conditions. The theoretical results agree with simulations on BA Networks.

Keywords: networks, routing, congestion, Markov process

INTRODUCTION

Overview

With the development of information age, the increasing of network scale and the expanding of network function, studies of network structure, performance and dynamics have gained more and more attention. As network research springs up, a variety of routings on complex networks have been proposed. They can be divided into four categories:

1. local static routing, based on local structure information of network (e.g. degree), open-loop system (non-feedback)
2. local dynamic routing, based on local state information (e.g. queue length), close-loop (Feedback)
3. global static routing, based on entire (or a significant portion of) network structure information, open-loop system (non-feedback)
4. global dynamic routing, based on state information of entire (or a significant portion of) network, close-loop (feedback)

In terms of packets transmission performance, global dynamic routings are the best, for the routings are derived from the entire structure of network with real-time feedback, which equals to give us a lot of extra information. However, with the increase of the scale of various communication networks in reality and with the appearance of some special networks (e.g. wireless Self-organizing networks), it is impossible for people to know entire or almost entire structure of a network, so that the local routings are especially important. We need a great amount of real-time communications if we use a close-loop routing which may increase the burden of network transmission. Therefore, there are special values in finding a high-performance open-loop routing, especially in some networks with limited communication abilities.

In the face of various routings proposed, there is a question: Given a certain network, respectively in four kinds of routings, how good can the optimal routing of each kind be? How can we find them?

In this paper, we study the congestion characteristics of a routing on a network. We use transmission capacity of the data packets ($R_c$) to measure it and analyze the routings using Markov process. We present the upper bound of $R_c$ of all static routings and estimate the divergence speed of it as network scale $N$ increases.

Models and routing rules

In a communication network, information (data) is transmitted in packets. Each device with the ability of data packets generating, delivering, receiving and analyzing abilities (routers in Computer communication network, agents in wireless communication networks) is abstracted into a vertex in this model. The physical connections between them correspond to edges between the vertexes. Consequently, the networks in the model reflect the topological properties of real networks. The same model is used here as in [1–5].

The packet transmission rules in the model are as follow:

Each time step, we select $C$ (if less then $C$, then all) data packets from the head of the queue of each vertex's cache and transfer them to their neighbors (vertexes with edges connecting each other). Meanwhile, $R$ new data packets are generated in the network. Each packet is born randomly at any vertex and randomly selects a vertex as the destination (except the vertex itself). The cache of each vertex is a queue structure and the new coming packets are placed at the end of the queue (FIFO). In addition, if a packet comes from any vertex $i$, then the next $n$ steps, the packet does not return to $i$, we call it $n - avoiding$. When $n$ is small, especially for the routing on sparse networks with large $R_c$, the effect of $n - avoiding$ is always a small quantity. Thus, in this paper, we set $n = 0$ in analysis and $n = 1$ in simulations on BA networks.

The arrival principle is as follows:

If a packet arrives at the neighbor of its target vertex (destination), it will be transferred to the target vertex at next step. If a packet arrives at its target vertex, it will be removed from the network.

The static routing is as follows:
for any vertex $i$, at any step $t$, we transfer the data packets at the head of the queue of $i$’s cache to the vertex’s neighbours vertex $j$ ($j = 1, 2, 3$) with probability $p_{ij}$, when the target vertexes of these packets are not vertex $i$’s neighbours. Transition matrix $P = (p_{ij})_{n \times n}$ is given by local information of network structure. If $p_{ij}$ is related to $t$ and $P(t) = (p_{ij}(t))_{n \times n}$ (usually $P$ is not explicitly a function of $t$ and relies on $t$ through system states), we call it local dynamic routing. If $p_{ij}$ is related to target vertex $x$ and $P = (p_{ijx})_{n \times n \times n \times n}$ is given by global information of network structure, we call it global static routing. If $p_{ij}$ is related to $t$ and $x$, and $P = (p_{ijx}(t))_{n \times n \times n \times n}$, we call it global dynamic routing.

The definition of various routings in this paper is a widespread frame type definition. Almost all the routing strategies studied till now can be included in our frame. Such definition shows significance to comprehend the essence of routing problems.

The meaning of transition matrix $P$ here is: bandwidth. A bandwidth refers to the maximum amount of information transferring through a channel per unit time. There is a little difference between this definition and what we discuss here. In this paper, the bandwidth means average bandwidth, which is the average amount of information transferring through a channel per unit time. Here, bandwidth is not only determined by the physical properties of a channel. We can properly design the allocation of the bandwidth of the whole network, which means we can design the amount of information transferring through a channel per unit time manually.

In fact, the problem, finding optimal routing, is a process of optimization of network bandwidth allocation. For local routing strategies, the method is obvious. For global routing strategies, we can solve it form different methods such as finding the optimal path by different meanings and generating the corresponding routing table. At the time when the routing table is generated and the packet generation rate of each vertex is given, a bandwidth allocation is already determined. Through different routing algorithm, we can get difference routing strategies and naturally generate different allocations of the bandwidth.

Model assumptions: 1. Network structure is constant or slowly varying. 2. The cache of the device is large enough that ‘out of memory’ will not happen. 3. Packets born time is stable. 4. Data packets are uniformly born in each vertex, and equiprobably choose their target vertexes. When $R$ is relatively small, as time goes on, the total number of data packets in network (the number of packets that has not yet arrived at the target vertexes at the current time) will reach a constant. This constant is of course limited, which has been supported by the results of computer simulations. The dynamic progress that can reach a stationary state like this is called free flow phase. However, when $R$ is relatively large, precisely, $R$ is larger than some $R_c$, the number of packets in network will increase with time and tend to infinity.

Such dynamic process is called congestion flow phase. We measure network transmission capacity ($R_c$) by whether there is congestion or not. Quantitatively, $R_c$ is defined as the transition point of order parameter $\eta$.

$$\eta = \lim_{t \rightarrow \infty} \frac{C \Delta W}{R \Delta t}$$

where $\Delta W = W(t + \Delta T) - W(t)$ expressed the number of data packets in network at $t$ time step. Our mission is under limited information, making $R_c$ as large as possible. In fact, $R_c$ always affects another quantity-average transmission time $T$. Precisely, we should find maximum $R_c$ with limited information and given $T$.

**MODEL ANALYSIS**

**Analytical method and some results**

First we have the follow conclusion: When the system has reached its stationary state, given a packet whose target(or birth vertex) is a certain vertex, the probability of finding it in any position of a queue of a given vertex is equal. Because when the system reaches a stationary state, it is a non time varying stochastic system. Let $\alpha_{ij}$ means after the system reaches the stationary state, at the head of the queue of vertex $i$, the probability of finding a packet whose target is vertex $j$. We use the relation that in average, the packet numbers of arriving and leaving are equal for stationary state, then we get the following equation:

$$\alpha_{ij} = \sum_k p_{ki} \alpha_{kj} (1 - a_{kj}) + \frac{R}{CN(N - 1)}, i \neq j$$

$$\alpha_{ii} = 0$$

So

$$\alpha = P^T \alpha - P^T (A \circ \alpha) + \frac{RJ}{C}$$

(1)

Where, $P, J, A$ refer to square matrices of order $N$. $P$ is a transition matrix. $P^T$ refers to the transpose of $P$. $A$ refers to an adjacency matrix of network. $\circ$ means Hadamard product. Each element of the Hadamard product of two matrices is the product of the corresponding elements of the two matrices. $Ca$ suggests the leaving packets each step. $P^T \alpha - P^T (A \circ \alpha)$ suggests the incoming packets, where $-P^T (A \circ \alpha)$ suggests that if a packet arrives at its target’s neighbours, it will be directly transferred to its target. $J$ is a born matrix. $RJ_{ij}$ is expectation of the number of packets born in vertex $i$ whose target vertexes are vertex
we have:

$$J = \frac{1}{(N-1)N} \begin{pmatrix}
0 & 1 & \cdots & 1 \\
1 & \ddots & \ddots & \vdots \\
\vdots & \ddots & \ddots & 1 \\
1 & \cdots & 1 & 0
\end{pmatrix}$$

With both sides divided by \( \frac{R}{C} \), Eq.(1) can be rewritten as:

$$\alpha_0 = P^T \alpha_0 - P^T \left( A \circ \alpha_0 \right) + J \tag{2}$$

where \( \alpha_0 = \frac{C \alpha}{R} \). We suppose:

$$Pd_i = (I - \text{diag}(a_{i1}, a_{i2}, \ldots, a_{iN}))P \tag{3}$$

where \( I \) refers to \( N \) order unit matrix. This operation sets the corresponding rows of vertex \( i \) and its neighbours to zero in matrix \( P \). The physical meanings are obvious: When a packet whose target is vertex \( i \) arrives at vertex \( i \) or its neighbours, it will not be transferred to any vertices expect vertex \( i \) and will be immediately removed from network (After arriving the target vertex), let column \( i \) of matrix \( \alpha_0 \) be \( \beta_{0i} \), column \( i \) of matrix \( J \) be \( J_i \):

$$\beta_{0i} = Pd_i^T \beta_{0i} + J_i$$

that is:

$$\beta_{0i} = (I - Pd_i^T)^{-1}J_i = (I + Pd_i^T + (Pd_i^T)^2 + \cdots)J_i, \quad i = 1, 2, 3 \ldots, N \tag{4}$$

For any \( i \), if and only if the series of Eq.(4) converges, Eq.(2) has a unique solution.

A sufficient condition of the convergence is: the graphs with adjacency matrix \( A \) and \( P \) are strongly connected. This is a natural requirement the problem we study must satisfy.

If and only if \( a_{ij} \neq 0, p_{ij} \neq 0 \). Then we say non-negative matrix \( P \) is consistent with \( A \).

In this paper, we only discuss the situation that Eq.(2) has a unique solution.

From Eq.(1), its easy to know the solution of the Eq.(2): all the elements of matrix \( \alpha_0 \) are non-negative.

Let row \( i \) of \( \alpha \) be \( \alpha_i \), then \( s_i = \alpha_i \times 1 \) presents the probability of the existence of packets at the head of queue of vertex \( i \) after the process reaching a stationary state. So, the requirement that there is a stationary state is: \( \max\{s_i\} \leq 1 \), the critical state satisfies \( \max\{s_i\} = 1 \), equivalently, \( \|\alpha\|_{\infty} = 1 \). Here \( Rc = C/\|\alpha_0\|_{\infty} \).

Now, we have analyzed network transmission capacity \( Rc \). Given an adjacency matrix presenting network structure information and a transition matrix \( P \) presenting routing strategy, we can calculate \( Rc \) using Eq.(2).

Let the average transmission time of packets be \( T \), we have:

$$T = 1^T \sum_u \left[ u \times ((Pd^T_u)^{u-1} - (Pd^T_u)^u)J_u \right] 1$$

$$= \sum_{ij} \alpha_{0i} = 1^T \alpha_{01}$$

where \( 1^T \) refers to \( (1 1 1 \cdots 1) \). Accordingly, the average transmission time of packets whose targets are vertex \( s \) is:

$$T_s = N \times 1^T \sum_u \left[ u \times ((Pd^T_s)^{u-1} - (Pd^T_s)^u) \right] J_s = N 1^T \beta_{0s}$$

Now, we surprisingly find the significance of matrix \( \alpha_0 \). The reciprocal of the sum of its maximum line reflects the network transmission capacity. While the sum of each row multiplying the vertex number \( N \) equals to the average transmission time of the packets whose target is the corresponding vertex. Transmission capacity and average time are two of the most important indices of transmission properties of network. Matrix \( \alpha_0 \) can describe these two clearly and can also quantitatively present the relation between them.

According to the meaning of \( \alpha_{ij} \) and the uniformity assumption above, approximately we have:

$$L_i = C \times s_i$$

where \( L_i \) represents the average queue length of vertex \( i \) after reaching the stationary state.

The whole length

$$L = \sum_i L_i$$

So

$$\frac{L}{R} = \sum_{ij} \alpha_{0ij} = T \tag{5}$$

These represent the relation among the transmission time of packets (waiting time), number of data packets born per time and length of queue of each vertex. This relation agrees with the classical conclusion[11][12].

When the network size \( N \) is large, in Eq.(1), the elements of matrix \( J \) tend to zero at the speed of \( 1/N \) and the elements of \( \alpha \) are at the magnitude of \( 1/N \). The number of subtrahends in Eq.(3) proportion of the total element also tends to zero at the speed of \( 1/N \) and \( R \) is remarkably less than \( Rc \). Eq.(1) asymptotically becomes \( \alpha_1 = P^T \alpha_1 \) with \( N \) increasing.

The solution of \( \alpha_1 = P^T \alpha_1 \) is the stationary distribution of Markov process \( P \) (differing from a positive scale coefficient). We sign the stationary distribution as \( \pi = (\pi_1, \pi_2, \pi_3, \cdots, \pi_n) \). Then \( L_i \propto \pi_i \) Rewrite Eq.(5) into

$$T = \frac{C}{\pi m Rc} \tag{6}$$
necessary prerequisite for Eq.(1)(3)(4)(7).

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m
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In order to see the essence clearly, we let

Rc0 = \frac{RC}{C}, T0 = \frac{T}{N}

Then Eq.(6) becomes

Rc0 = \frac{1}{T0 N \pi_m}

For \pi_m \geq 1/N, we have \(\Rc_0 \leq 1/T_0\), equivalently

T_0 \Rc_0 \leq 1 \quad (7)

Eq.(7) is the constraint relations between average trans-
mission time and transmission capacity.

Therefore, there is a contradiction between transmission
time and transmission capacity. If we want less time, we
may not have high transmission capacity. If we want high
transmission capacity, we may fail to deliver the packets
quickly. This is consistent with the physical intuition.

We should find a routing that can relieve the congestion
while considering the transmission time [13, 14].

Eq.(6) and Eq.(7) seem to suggest : When the station-
ary distribution of the load of each vertex is near uniform,
the corresponding routing, or the corresponding matrix
P may have a good transmission capability. A network
with the routing of a doubly-stochastic matrix whose sta-
tionary distribution \(\pi_i = 1/N = \pi_m\) should have a good
transmission capability. The doubly stochastic matrix
refers to a transition matrix that the sum of rows and
columns are both 1[15].while Scale-Free networks are lit-
tle homogeneous for the degree of each vertex differs a
lot.

It should be noted that, although in this paper we study
scale-free networks as an example, scale-free is not is a
necessary prerequisite for Eq.[13, 14, 17).

The Estimate of optimum and upper bond

As mentioned above, there is a contradiction between transmission
accuracy and transmission capacity. Only after
given one of them we can compare it with the other.

Computer simulation results show that, for a given net-
work, given \(T_0\), we can optimize the transmission capaci-
ity \(\Rc_0\) of a local static routing. We denote the maximum
\(\Rc_0\) as \(\Rc_{0m}\). Obviously, \(\Rc_{0m}\) is a function of \(T_0\). With
the variation of \(T_0\), it is certain that the maximum of
\(\Rc_{0m}\) exists because the function is bounded.

Fig[3] show us: although the routing with best con-
gestion characteristics (max \(\Rc\)) is a routing that each
vertex loads uniformly, it is not a completely uniform
load routing.

Whether a routing with completely uniform load exists
in a network (if and only if \(T_0 \Rc_0 = 1\)) and what value
\(T_0\) can be are related to the structure of the network.

Next we estimation the upper bound of \(\Rc\) of the local
routing.

When any \(k_i/N\) is an infinitesimal,for sparse networks
with very large scale \(N\), \(\text{(number of all edges}/N < \text{some finite constant})\), there is few differences between
\(Pd_i\) and \(P\). So we have the approximation: \(Pd_i^T \pi \approx C_i \pi\),
where \(\pi\) refers to the stationary distribution of \(P\) and \(C_i\)
refers to a positive constant near 1. Considering that we
want a routing with large \(\Rc\), many computer simulation
experiments tell us that the loads with the routing are
nearly uniform when \(\Rc\) is larger, that is :the angle
between the all 1 vector and \(\pi\) is lesser.

Basing on the above two conclusions, we approximately have:

\(\frac{(Pd_i^T)^n}{N} \approx (1^T Pd_i^T \pi)^n \pi\)

With this approximation, we have:

\(\Rc_0 = \frac{N}{\pi_m} (1/\sum_j a_{ij} \pi_j) \leq \frac{1}{<1/k>} \leq <k>\)

Where \(<1/k>\) refers to the average of degrees reciprocals
and \(<k>\) refers to average degree. For large BA net-
works, we have \(1/\sqrt{k} \approx 3 <k> /4[16, 17]\). In fact,
\(\pi_m \sum_i (1/\sum_j a_{ij} \pi_j)\) has a clear physical
meaning.

Here can we make an extrapolation of the results? If
a vertex knows the information of its neighbours around
within \(n\) layers (\(n\) is not very large), do we have the con-
clusion \(\Rc \leq 1/\sqrt{n}\)? A vertex’s neighbours around
within \(n\) layers mentioned here is the vertexes that the
shortest distance between which and that vertex is \(n\).
\(k^{(n)}\) refers to \(n\)-layer degree. This extrapolation needs
further work to prove.
are born in vertex

fixed transmission path or 'link' for any packets which

global information[1, 5, 13, 14]. Simply put, there is a

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[1] define these metrics by vertex degree , [5] define these

link length in different ways, we get the shortest path

'link' is the shortest path in some sense. Measuring the

vertex (destination) between analysis and simulation, and the sta tionary distribution of the transition matrix by

SLR. FIG.2.b shows the comparison of the average transmission time of each vertex (destination) between analysis

and simulation. In FIG.2.a, the graphs of analysis and the stationary distribution of transition matrix are almost

overlapping. We normalize the data both in FIG.2.a and b by their own me an value.

GLOBAL STATIC ROUTING AND

BETWEENNESS

The shortest path routing widely used in network com-

munication is a 'Link Type’ routing strategy based on
global information[1, 5, 13, 14]. Simply put, there is a

fixed transmission path or ‘link' for any packets which

are born in vertex i and whose target is vertex j. Each

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course, these routings all belong to the frame type defini-

tion we mention above. There is a a one-to-one relation-

ship between the language of ‘link’ and the language of

transition matrix for a routing.

Considering a global static routing, now we suppose the

routing has been converted into the language of transition

matrix. As mentioned above, we have N transition

matrices \{P_1, P_2, P_3 \ldots P_N\}. \ P_i refers to transition ma-

trix that is used in transferring packets whose target is

vertex i. Then according to the approximation above, let:

\[ P'_i = (I - \text{diag}(a_{i1}, a_{i2} \ldots a_{iN})) P_i \]

then

\[ \beta_{0i} = (I - P'_i)^{-1} J_i \]

That is to say, the global routing has N transition ma-

trix rather than 1, which is different from the local rout-

ing. However, \( Rc = C/\|a_0\|_\infty, \quad T = \sum_i \sum_j a_{0ij} \) these two

equations are still true. Thus, we present a unified solu-

tion for local and global routing.

For the analysis of \( Rc \) of global routing, paper [1] present

the results:

\[ Rc = \frac{CN(N-1)}{B_{max}} \]

where \( B_{max} \) refers to the maximum betweenness. Be-

tweenness of a vertex is the number of paths through the

vertex.(Strictly, we should consider the probability going

through each vertex, but it makes no difference) Actually,

this result matches ours. We can get the betweenness of

vertex i ,that is : \( Bi = N(N-1)s_{0i} \) by simple calcula-
tions.Here \( s_{0i} \) refers to the sum of all elements of ith row

of matrix \( a_0 \).Thus, we can define betweenness in local

routings the same as in global routings.

Now we rewrite the results in local static routings we
FIG. 3: a (color online) The numbers of vertexes and edges of networks NW 1 ∼ 3 are equal, but the maximum transmission capacity of these three networks are totally different. The average length of shortest paths of NW1 is the shortest among them three, so \( T_0 \) can be very small. However, there exists a hub vertex which seriously limited the transmission capacity. Comparing NW3 and NW2, we further reduce the hub property of the centre point of NW2, and improve the transmission capacity a little.

b (color online) The numbers of vertexes, edges and the average length of shortest paths of networks NW4 ∼ 7 are equal, but the graphs of NW7 and NW4 ∼ 6 differ a lot. Here we can see: the critical point of the congestion is the vertex in the middle. There is little difference if we change the network structure except the middle vertex. Only when we reduce the hub property of the hub vertex, can we improve the transmission performance greatly.

FIG. 4: The ordinate is from Eq. (2) and the abscissa is the approximate solution of it under the two approximate conditions above. With each parameter, we randomly generate 100 BA networks and 20 transition matrices for each. Thus, we have 2000 data points for each parameter in the graph, the black full line is diagonal, and data points are scattered near it, which supports the validity of approximation. When the network scale is not large but the average degree is not small (e.g. \( N = 200, k = 14 \)), the data points are scattered widely. It also suggests that we can only approximately determine \( Rc \) by stationary distribution and network structure for large sparse networks. is approximately proportional to betweenness.

\[
\pi_i = \frac{B_i}{\sum_j B_j}
\]

Here we can see more clearly, betweenness is consistent with stationary distribution in Markov process, which represent the average number of times that packets go through some vertex per unit time.

It is worth emphasizing that we take the approximation that using ‘transmission hops’ instead of ‘transmission time’in the equations expressed in betweenness above. So there is some deviation. However, as the assumptions that satisfies Eq. (2) above, this deviation will not be unacceptable most of the time. Significantly, these equations expressed in betweenness are enough to describe the variation of these important variables with different parameters, whatever the accuracy.

It is not difficult for us to derive that in global routings, we also have the equation:

\[
T_0 Rc_0 \leq 1
\]

The equation is the same as that in local routing. When the queue length of each vertex tends to be equal, the inequation becomes an equation.
For local routing, when $T_0$ is small, there may not exist any routings with which the queue lengths tend to be uniform. For global routings, when $T_0$ is small, there may still exist such routings. This illustrate the reason why transmission capacity of global routings can be much higher than that of local routings from a point of view.

Next, we give an estimate of the upper bound of the divergence speed of global routing $R_c$ with $N$. From Eq. 5 we know $R_c \leq CN(N-1)/B$, $B$ is larger than average betweenness $B_0$ in the shortest path routing strategy. Let the network average shortest path length be $Z$. We have $B_0 = (N-1)Z$ (more generally, if packets are not born in each vertex equiprobably, we should calculate it from weighted averages)

$$R_c \leq CN/Z$$

(9)

That is to say, $R_c$ is limited by network average shortest path length. Similarly, average transmission time $T \geq Z$. The significance of Eq. 9 is that a network with shorter diameter may always have better a transmission performance. This is not an absolute conclusion, because, if there are many vertexes with large degree in a network, they may form some congestion centers and the transmission capability may be limited. If a network does not have small world characteristics, which means $Z \sim N$, with the increasing of $N$, $R_c$ will be limited by a constant. When a network has small word characteristics, which means $Z \sim N^r$, $0 < r < 1$, with $N$ tending to infinity, $R_c$ tends to infinity. Specially, for BA networks, roughly speaking, we have $Z \sim \log N/\log \log N$ [16, 21, 22]. Then divergence speed of $R_c$ will be limited by $N \log \log N / \log N$ with $N$ increasing to infinity. Although the above discussion is on static routings, when a dynamic routing (approximately) tends to a stationary state (transition matrix of which tends to be some constant matrix), our method is still suitable. The reason why dynamic routings have better performance than static routings is that dynamic routings have better adjustability (more parameters and more information). Besides helping us to find a routing with better performance, the better adjustability leads to the better adaptability to transmission conditions. Thus dynamic routings are more practical. Tending to a stationary state is often a basic requirement for a dynamic routing, for people need stable transmission. Thus, the significance of our paper is not only limited in static routings.

**CONCLUSION**

The problem of data transmission on network is essentially a problem of a queuing system. We are not the first ones to use Markov processes in modeling of queuing systems. It is a successful application of Markov processes in this paper and we get some new and basic results. For all local and global static routings, we get a universal inequality $R_c T_0 \leq 1$. For all local static routings, with certain assumption, we have $R_c / (1/k) > 0 .