Three-Dimensional Carbon Allotropes Comprising Phenyl Rings and Acetylenic Chains in $sp^+sp^2$ Hybrid Networks

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We here identify by ab initio calculations a new type of three-dimensional (3D) carbon allotropes that consist of phenyl rings connected by linear acetylenic chains in $sp^+sp^2$ bonding networks. These structures are constructed by inserting acetylenic or diacetylenic bonds into an all $sp^2$-hybridized rhombohedral polybenzene lattice, and the resulting 3D phenylacetylene and phenyldiacetylene nets comprise a 12-atom and 18-atom rhombohedral primitive unit cells in the $R3m$ symmetry, which are characterized as the 3D chiral crystalline modification of 2D graphyne and graphdiyne, respectively. Simulated phonon spectra reveal that these structures are dynamically stable. Electronic band calculations indicate that phenylacetylene is metallic, while phenyldiacetylene is a semiconductor with an indirect band gap of 0.58 eV. The present results establish a new type of carbon phases and offer insights into their outstanding structural and electronic properties.

The valence electrons of carbon atom are capable of forming $sp^3$, $sp^2$- and $sp^1$-hybridized states that support four basic types of single, double, triple, and aromatic carbon-carbon bonds1–4. These different bonding states in various compounds have a profound impact on a wide range of properties of carbon-based materials. At ambient conditions, graphite, which is structurally related to polycyclic benzenoid aromatic hydrocarbon, is the thermodynamically most stable carbon configuration. The polycyclic carbon atoms form a two-dimensional (2D) benzenoid $sp^2$ bonding network with a bond angle of 120° and a bond length of 0.142 nm. Diamond, which is related to polycyclic saturated hydrocarbon, is the second most stable allotrope of carbon with all the carbon atoms in a methane-like tetrahedral $sp^3$ bonding state with a bond angle of 109.5° and a bond length of 0.154 nm as in alkanes, forming a very rigid three-dimensional (3D) carbon network. Linear carbyne, which is related to polyyne-like unsaturated hydrocarbon with alternating single and triple carbon-carbon bonds rather than a cumulene structure, forming the simplest one-dimensional (1D) carbon chain, and it has been recently synthesized1, despite its rather high energy of about 1 eV per atom above that of graphite.

Since the discovery of fullerenes2, nanotubes3, and graphene4, considerable theoretical and experimental efforts have been made to search and assess new potential carbon allotropes5–20. Intriguing among them are the so-called graphyne and graphdiyne21–24, which are constructed by replacing one-third of the C–C bonds in graphene sheet with acetylenic (–C≡C–) or diacetylenic (–C≡C–C≡C–) linkages. Analogously, graphyne nanotubes25 and fullereneynes26 are also proposed theoretically. Thus far, large-scale graphyne and graphdiyne films composed of $sp^+sp^2$ hybrid network27–29 have been successfully synthesized under laboratory conditions. Motivated by $sp^+sp^2$-hybridized 2D carbon allotropes, an $sp^+sp^3$-hybridized 3D diamondyne was suggested by inserting triple yne-bonds into all the C–C bonds in cubic diamond30–32. In addition, a new material termed

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Figure 1. Three-dimensional carbon networks of rh6 polybenzene and polybenzene-ynes with phenylic rings and acetylenic chains in R3m (D12d) symmetry. (a) Rh6 polybenzene in an all sp2 3D bonding network with lattice parameters a = 6.9022 Å, c = 3.470 Å, occupying the 18h (0.8805, 0.1195, 0.5576) position, which comprises three zigzag benzene rings as its building blocks. (b) Rh12 phenylacetylene with lattice parameters a = 11.605 Å and c = 3.6443 Å. The 18h1 (0.8579, 0.9289, 0.4849) atoms form three benzene rings and 18h2 (0.8617, 0.7233, 0.6021) atoms form nine acetylenic yne-bonds located between the benzene rings. (c) Rh18 phenyldiacetylene with lattice parameters a = 16.0963 Å and c = 4.1987 Å. The atoms on 18h1 (0.1023, 0.0511, 0.5065) site form three benzene rings; The atoms on 18h2 (0.1008, 0.8992, 0.4507) and 18h3 (0.1435, 0.8565, 0.3755) sites form nine butadiyne located between the benzene rings. The primitive cell is marked by yellow lines.
between the benzene rings. Note that the carbon chains are not perfectly linear with the bond angles of 172.54° for ∠C1–C2–C3 and 180° for ∠C2–C3–C3. In the rhombohedral representation, it has an 18-atom primitive unit cell, thus it is termed as rh18 carbon. The two new structures introduced here represent a new type of carbon allotropes that consist of phenyl rings connected by linear acetylenic chains in sp2 bonding networks.

The total energies of rh12 phenylacetylene and rh18 phenyldiacetylene as a function of volume are shown in Fig. 2 in comparison with the results for diamond, graphite, rh6 carbon, carbyne, and diamondyne. Our calculated energetic data establish the stability sequence: diamondyne < carbyne < rh18 < rh12 < rh6. It is clearly seen that the rh12 and rh18 polybenzeneynes are located between the energy range for rh6 carbon and carbyne, with an energy gain of about 0.07 eV per atom, while the diamondyne is out of the energy range, and even less favorable than carbyne.

By fitting the calculated total energy as a function of volume to Murnaghan’s equation of state42, we obtain the bulk modulus (B0) of rh12 and rh18 carbon as 195 and 129 GPa, respectively. The atomic densities are estimated to be 2.50, 1.69, and 1.14 g/cm3 for rh6, rh12, and rh18 carbon, respectively, which are considerably different from 3.51 g/cm3 for diamond and 2.27 g/cm3 for graphite. We can see that with increasing of the acetylenic chain length, the atomic density and bulk modulus are decreasing to a level even lower than those of graphite. The calculated equilibrium structural parameters, total energy, and bulk modulus for diamond, rh6 polybenzene, rh12-phenylacetylene, rh18-phenyldiacetylene, and graphite are listed in Table 1 and compared to available experimental data43.

We next examine the dynamic stability of the 3D sp + sp2 bonding networks by phonon mode analysis. Figure 3a shows the phonon band structures and density of state (DOS) for the 3D phenylacetylene. The obtained phonon eigenvalues can be explained well by considering the bonding nature of the phenyl and triple carbon-carbon bonds. The vibrational modes due to the triple yne-bond can be observed clearly around 2150 cm−1 with the carbon-carbon bond length of 1.232 Å (C1–C2) and the vibrational modes due to the phenyl bonds are distributed around 1500 cm−1 with the carbon-carbon bond length of 1.433 Å (C1–C3). The combination modes of phenyl and triple bonds of carbon atoms can be seen clearly below 730 cm−1. No imaginary frequencies were observed throughout the entire phonon band structures, thus confirming the dynamic stability of the 3D-phenylacetylene. Meanwhile, there is a large phonon band gap in the frequency range of 1500 cm−1.
and 2100 cm$^{-1}$. Similar dynamic stability and vibrational modes are also confirmed for 3D phenyldiacetylene as shown in Fig. 3b. However, in the latter case there are two yne-modes around 2148 and 2193 cm$^{-1}$ due to the diyne bonds related to the C$_2$ and C$_3$ carbon atoms.

To further examine the thermal stability, we have also performed ab initio molecular dynamics simulations using a $1 \times 1 \times 2$ hexagonal supercell, which contains 6 primitive cells. After being heated at room temperature (300 K) and 1000 K for 3 ps with a time step of 1 fs, no structural changes occurred for both rh12 and rh18 carbon. These results show that rh12 and rh18 carbon are viable carbon allotrope for experimental synthesis.

Figure 3. Phonon band structures and partial density of states (DOS). Results for rh12 phenylacetylene (a) and rh18 phenyldiacetylene (b). The spectra due to the triple bonds and phenyl bonds occur around 2150 cm$^{-1}$ and 1500 cm$^{-1}$, respectively. A clearer picture for the low vibrational modes is given in Fig. S1 in Supplementary Information.
Figure 4 shows the calculated electronic band structures and projected density of states (PDOS) by using the hybrid functionals (HSE06)\textsuperscript{39}. The calculated band gap for diamond is about 5.36 eV, which is closed to the experimental data of 5.47 eV\textsuperscript{43}, indicating the validity of the HSE06 method in predicting the band gaps for diamond and related sp\textsuperscript{3} bonded carbon structures. For 3D-phenylacetylene, as shown in Fig. 4a, there are three bands around the A, K and M points across the Fermi level, resulting in the metallic nature of the system. Meanwhile, for 3D-phenyldiacetylene, as shown in Fig. 4b, the conduction band minimum and valence band maximum are located at the L and Γ point, respectively, showing a semiconductor character with an indirect band gap of 0.58 eV. Moreover, from the PDOS, we can see that the states around the Fermi level are mainly coming from the 2p orbitals, which define the metallic nature for phenylacetylene and the band gap for phenyldiacetylene.

To understand the bonding nature of electrons in both rh12 and rh18 carbon, the electron density difference (EDD) and electron localization function (ELF) maps are illustrated in Fig. 5. The EDD maps represent the variation of electron density in terms of chemical bonding. One can make an EDD plot by subtracting the overlapping...
atomic electron density from the self-consistent electron density of a crystal. The ELF maps can give a clear and quantitative description on the basic chemical bond (high ELF values > 0.5 indicate the formation of covalent bonds)\(^{44-46}\), which was initially proposed by Becke and Edgecombe\(^{45}\) based on Hartree-Fock theory, and generalized by Savin \textit{et al.}\(^{46}\) based on density functional theory. From the EDD maps shown in Fig. 5a,b, we can see that there is a larger gain of electron density between triple bonded carbons. Meanwhile, from the ELF maps shown in Fig. 5c,d, we can see that the electrons are well localized along the carbon chain, and the enhanced localization between triple bonded carbons can be seen clearly, which is more than the localization between the single and aromatic bonded carbons. These results show the strong triple bonding nature in the \(sp^3\) hybrid networks.

Furthermore, to understand the aromaticity in the phenyl rings, the nuclear-independent chemical shift NICS(0) at the center of the phenyl rings are calculated using the gauge-including atomic orbital (GIAO) method at the B3LYP/6-311 + G(d,p) level\(^ {47}\). The NICS(0) values are estimated to be \(-8.16\) ppm for benzene, \(-5.23\) ppm for rh12 carbon, and \(-6.57\) ppm for rh18 carbon. These results show that the aromaticity in phenyl rings of rh12 and rh18 carbon are smaller than the aromaticity in benzene.

Finally, we plot in Fig. 6a simulated x-ray diffraction (XRD) patterns for graphite, diamond, rh6 polybenzene, rh12 phenylacetylene, rh18 phenyldiacetylene and and fcc C\(_{60}\) compared to the experimental data for chimney soot and detonation soot\(^ {48}\). It is shown that the main (101) peak at 30° for rh6 should shift to 26° for rh12 and 22.4° for rh18 carbon. The main (101) peak at 26° for rh12 is very close to the main (002) peak at 26.5° for graphite, thus rh12 carbon may coexist with graphite in the detonation soot (see Fig. 6b and the Fig. 2 in ref. 48). On the other hand, for chimney soot, as shown in Fig. 6b, there is a sharp peak at 29.8°, which is fit well by the rh6 (101) diffraction peak, while a broad diffraction around 23°, which matches the rh18 (101) diffraction peak. These

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**Figure 5.** Electron density difference and electron localization function maps. (a,b) The electron density difference (EDD) for rh12 carbon (a) and rh18 carbon (b) with an isodensity of 0.1 e/Å\(^3\). The blue colour denotes a gain and the yellow colour a loss of electron density. (c,d) The electron localization function (ELF) for rh12 carbon (c) and rh18 carbon (d) with an isosurface level of 0.75.
results suggest that rh12 and rh18 carbon as well as rh6 carbon may be present in chimney soot, carbon black or detonation soot.

**Conclusions**

In conclusion, we have identified by **ab initio** calculations a new type of three-dimensional carbon allotropes that consist of phenyl rings connected by linear acetylenic chains in \( sp^2 \) bonding networks. The resulting 3D phenylacetylene and phenyldiacetylene network structures in \( R m (D_{2d}^5) \) symmetry are topologically corresponding to 2D graphyne and graphdiyne, respectively, and they are energetically more favorable than the \( sp^2 \)-hybridized 1D carbyne chains and the recently reported \( sp^3 \)-hybridized 3D diamondyne. Phonon calculations show that these newly predicted structures are all dynamically stable. Electronic band and density of states calculations indicate that 3D-phenylacetylene with acetylenic yne-bonds is metallic, while 3D-phenyldiacetylene with diacetylenic yne-bonds is a semiconductor with an indirect band gap of 0.58 eV. Moreover, a detailed XRD analysis shows that phenylacetylene and phenyldiacetylene 3D network structures as well as rh6 polybenzene match the experimental diffraction peaks seen in the carbon black, diesel soot or chimney soot. Our findings suggest a novel strategy in constructing carbon framework structures that may help solve the structures of the newly discovered but unidentified carbon phases seen in recent detonation experiments.

**Methods**

Our calculations are carried out using the density functional theory as implemented in the Vienna **ab initio** simulation package (VASP). The generalized gradient approximation (GGA) developed by Armiento-Mattsson (AM05) were adopted for the exchange-correlation potential. The all-electron projector augmented wave (PAW) method was adopted with \( 2s2p^2 \) treated as valence electrons. A plane-wave basis set with a large energy cutoff of 800 eV was used. Forces on the ions are calculated through the Hellmann-Feynman theorem allowing a full geometry optimization. The energy minimization is done over the atomic and electronic degrees of freedom using the conjugate gradient iterative technique. Convergence criteria employed for both the electronic self-consistent relaxation and the ionic relaxation were set to \( 10^{-8} \) eV and 0.01 eV/Å for energy and force.

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**Figure 6. X-ray diffraction (XRD) patterns.** (a) Simulated XRD patterns for graphite, diamond, rh6 polybenzene, rh12 phenylacetylene, rh18 phenyldiacetylene, and fcc C_{60}. (b) Experimental XRD patterns for chimney soot and detonation soot. The black, green, and red arrows indicate the XRD peaks corresponding to the main peak for rh6, rh12, and rh18 carbon, respectively. X-ray wavelength is 1.5406 Å with a copper source.
respectively. A hybrid density functional method based on the Heyd-Scuseria-Ernzerhof scheme (HSE06)\(^3\) has been used to calculate electronic properties. Phonon calculations are performed using the phono code\(^3\) based on the supercell approach\(^4\) with a \((1 \times 1 \times 2)\) 72-atom atomic supercell for rh12 and a \((1 \times 1 \times 2)\) 108-atom hexagonal supercell for rh18 carbon. Ab initio molecular dynamics simulations under constant temperature (300 K and 1000 K) and volume (NVT) were performed to check thermal stability with a time step of 1 fs up to 3 ps. The nuclear-independent chemical shift NICS(0) at the center of the phenyl rings are calculated using the gauge-including atomic orbital (GIAO) method at the B3LYP/6-311 + G(d,p) level\(^7\) as implemented in Gaussian03.

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Author Contributions

J.-T.W., C.F.C., H.-D.L., H.M. and Y.K. designed the study and wrote the paper; J.-T.W. carried out *ab initio* simulations; all authors discussed the results and contributed to the manuscript.

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