Verification of a framework for cyclic p-y curves in clay by hindcast of Sabine River, SOLCYP and centrifuge laterally loaded pile tests

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\textbf{ABSTRACT}

Pile foundations supporting offshore structures, such as jacket platforms, are subjected to cyclic lateral loading. The capacity and deformation of these pile foundations under cyclic lateral loading are important and challenging design aspects. The purpose of this paper is to present verification of a framework for analysing the lateral pile response under cyclic loading in clay, based on fundamental soil behaviour measured in the laboratory at the element level. This framework can account for site-specific cyclic soil properties, summarized in classic contour diagrams, and the site-specific cyclic loading characteristics in design. This is a step-change improvement from current codes and standards recommendations which are based on a series of tests on a single pile at a single site (i.e. the Sabine River tests, Matlock 1962, 1970). The paper first provides a brief summary of the framework and outlines the important assumptions and calculation procedures. The paper then presents a comprehensive validation exercise of the framework through back-analyses of three sets of 1-g and centrifuge tests, covering different soil conditions (strength profile, OCR and plasticity) and loading sequences. This hindcast demonstrates the model’s capabilities to capture the essential behaviours of pile foundations under cyclic lateral loading and its added value as a design tool, when compared with current practice.

1. Introduction

Offshore pile foundations typically need to be designed for cyclic lateral loading. As per state-of-practice, this is commonly performed by carrying out beam-column analyses where the soil pile interaction is represented by series of p-y springs (curves) along the depth of the pile. For both design and assessment, Jeanjean et al. [11] emphasized the importance of using best-estimate p-y curves which represent the soil support as accurately as possible. The most widely used p-y curves in clay are the API RP 2GEO curves [10] which were developed from limited pile tests at the Sabine River site in the 1950s, as reported in Matlock [21]. The API recommendations have essentially been unchanged since 1972 [4]. Their limitations are widely recognised in the industry and discussed amongst others in Jeanjean [10], Jeanjean et al. [11], and Zhang et al. [26]. In particular, the API method approximates the soil stress-strain response in monotonic and cyclic loading through the UU triaxial test. The project-specific cyclic loading conditions (e.g. make-up of storm load history, ratio between cyclic and average loading) are also not accounted for and the API cyclic curves are intended as minimum backbone curves obtained after several hundreds of cycles [20].

The industry lacks practical design procedures that can explicitly account for project-specific soil and load conditions. Zhu et al. [33] proposed an empirical p-y model that can account for the impact of the number of cycles and the cyclic loading amplitude on the evolution of the p-y curves based on two field pile load tests in soft clay. However, the consideration of site specific soil stress-strain response remains simplistic. The approaches presented by Erbrich et al. [8] and Zhang et al. [26,28] are two exceptions, which allow for consideration of project-specific soil and load conditions. The similarities and differences between the two models are discussed in Zhang et al. [26]. Zhang et al. [26,28] presented validation of their model through finite element analyses. The motivation of this paper is to present physical validation of the model through a comprehensive back-analysis exercise of several sets of field and centrifuge tests to demonstrate the model’s ability to capture pile response under cyclic loading.

For completeness, the paper will first briefly describe the framework for calculating pile response under monotonic and cyclic pile head loading and will then report the back-analyses of the field and centrifuge tests.

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2. Description of the model

2.1. The monotonic \( p-y \) approach

Zhang and Andersen [29] and Jeanjean et al. [11] proposed frameworks to derive site-specific monotonic \( p-y \) curves by scaling the soil stress-strain response measured in Direct Simple Shear (DSS) tests, as illustrated in Fig. 1. For a point on the normalised stress-strain curve, Jeanjean et al. [11] showed that the two frameworks for scaling DSS curves into \( p-y \) curves give very similar results. The framework of Zhang and Andersen [29] was implemented in the beam-column software NGI-PILE and used in this work.

2.2. The cyclic \( p-y \) approach

Combining the concept of equivalent number of cycles \( N_{eq} \), which is defined as the number of cycles at the current load level that would have produced the same cyclic effects (changes in strength and stiffness) as by the actual previous cyclic load history, Zhang et al. [26,28] extended the above monotonic framework to the cyclic \( p-y \) response of piles. On a single pile element level, it is postulated that the cyclic effects due to lateral loading of a pile element under average \( p_u \) for \( N \) number of cycles is analogous to the shearing of a DSS soil element under stress \( \tau_{cy} \) for \( N_{eq} \) number of cycles if \( p_{cy}/p_u = \tau_{cy}/\gamma_{u} \), as illustrated in Fig. 2. By assuming so, a single \( N_{eq} \) can therefore be evaluated by the same strain accumulation procedure applicable for a DSS test, as described by Andersen [3]. For a pile element, if the previous loading history is equivalent to \( N_{eq} \) number of cycles at the current mobilisation level, the soil stress-strain response corresponding to \( N_{eq} \) can be derived from the cyclic strain contour diagram, which is established from cyclic soil element testing. By using the same scaling procedure used for monotonic \( p-y \) curves (i.e. [29]), the \( p-y \) curves for calculating the pile responses under the current cyclic loading can be derived.

Fig. 3 provides a schematic illustration of the concept. The figure illustrates a pile element with a combination of average and cyclic mobilisations equal to 0.2 and 0.4 of the static capacity, respectively, and \( N_{eq} = 10 \). Note that the cyclic mobilisation is defined as the mobilized soil pressure under the cyclic component of the pile load normalized by the ultimate static bearing pressure for the pile element in consideration. Similar definition applies to the average mobilisation level. The stress strain curves for average and cyclic components of loading can then be established by drawing a horizontal cross-section at \( \tau_{cy}/\gamma_{u} = 0.4 \) and a vertical cross-section at \( \tau_{u}/\gamma_{u} = 0.2 \) respectively. The

![Diagram](image_url)

**Fig. 1.** Illustration of framework for deriving monotonic \( p-y \) curves from stress-strain response measured in DSS tests [11,29].
cross-section lines intersect with the average or the cyclic strain contour lines, and the intersection points form the stress-strain curves.

Using these p-y curves, the pile response under the current load can be evaluated. Note that the total pile response (displacements and forces) is the sum of responses under average and cyclic components of the pile load. With the above assumptions, the pile response under a pile head load history can be analysed within the framework of a conventional beam-column p-y model, as schematically illustrated by Fig. 4. The design pile head load history is first sorted into load parcels with constant average and cyclic loads. The load history is then analysed in a parcel by parcel manner. The key is to keep track of the loading history for each of the p-y elements. By updating the global equilibrium and p-y springs at the beginning and at the end of each load parcel, the evolution of the pile response during the load history can be calculated. This procedure is explained in detail in Zhang et al. [28] and implemented in a computer program called NGI-PILE.

The cyclic framework described above has been validated by numerical analyses, firstly at a single pile element level (i.e. a horizontal pile slice) to verify the analogy illustrated in Fig. 2, and then for a complete pile to verify the calculation procedure and redistribution of loads along the pile under cyclic loading. These were performed in finite element analyses with the UDCAM cyclic accumulation soil model [12], which uses cyclic contour diagrams established from soil elements tests as input. In the analyses, the stress history at each integration point of the entire finite element soil domain was kept track of and the soil strength and stiffness at each point is constantly updated. The numerical validation exercise demonstrates excellent predictive capability the model and further details can be found in Zhang et al. [26,28].

2.3. Modelling of the pile-soil interface

The proposed model allows for explicit consideration of the pile-soil interface roughness. The interface roughness not only influences the ultimate capacity of the p-y spring [27], but also the stiffness [29]. The user of the model can therefore evaluate the interface roughness based on the soil profile, for example, according the axial capacity method recommended in API [5]. This also allows for the possibility to account for the effect of the pile installation method, which has an important

**Fig. 2.** Analogy between loading of a pile element and shearing of a DSS soil element [26].

**Fig. 3.** Schematic illustration on derivation of p-y curves for average and cyclic components of loading (modified from [28]).
2.4. Limitation

It should be noted that the monotonic and cyclic p-y framework outlined above is primarily developed for design of slender piles where the soil-pile interaction can be sufficiently captured by distributed p-y springs along the pile and a flow-around soil mechanism is dominating. For short stubby piles, such as monopiles supporting offshore wind turbines, additional components of soil resistance, such as base shear at pile tip and distributed moment due to vertical shear force along pile shaft, also need to be considered [6,32].

3. Validation of the model against physical pile testing

3.1. Overview

Several field and centrifuge tests reported in the literature are back-analysed in order to verify the proposed cyclic p-y framework. This includes the Sabine River tests [19], which formed the basis for development of the API p-y curves [21], and the Matlock p-y formulation in soft clays [22], which was adopted by API RP2A 3rd Edition [4] and still appears in API RP 2GEO [4]. The model pile had an outer diameter of 0.324 m, a uniform wall thickness of 12.7 mm, and a total length of 13.1 m. The pile was embedded 12.8 m below the ground surface so that the lateral load was applied 0.3 m above the ground surface. The model pile was instrumented with 35 pairs of strain gauges which measured the bending moment along the pile. The spacing between the gauges varied from 0.15 m near the top to 1.22 m in the lowest section.

The model pile was driven closed-ended to the target penetration by impact hammering. Four main tests were carried out at the Sabine River site, including two monotonic loading tests (one free head and one constrained head) and two cyclic loading tests (one free head and one constrained head). Due to the uncertainty with the exact level for fixity for the constrained pile head tests, only the two free head tests are back-analysed in the current exercise.

3.2. Sabine River field pile testing

3.2.1. Geometry and instrumentation

The Sabine River pile load tests are summarized in Matlock and Tucker [19] and analysed in Matlock [20]. These tests formed the primary basis of the “Matlock p-y formulation” in soft clays [21], which was adopted by API RP2A 3rd Edition [4] and still appears in API RP 2GEO [4]. The model pile had an outer diameter of 0.324 m, a uniform wall thickness of 12.7 mm, and a total length of 13.1 m. The pile was embedded 12.8 m below the ground surface so that the lateral load was applied 0.3 m above the ground surface. The model pile was instrumented with 35 pairs of strain gauges which measured the bending moment along the pile. The spacing between the gauges varied from 0.15 m near the top to 1.22 m in the lowest section.

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3.2.2. Soil condition

The tests were carried out at a site near the Sabine River mouth, which primarily consists of marine-deposited, high plasticity clay, but interbedded with thin silty sand and sand layers. A desiccated 1.38 m thick surface crust was excavated, below which a soft marine clay of high plasticity with water content close to the liquid limit values was present to a depth of 3 m. A clay with 25 mm to 100 mm thick seams of shelly sand occurred between depths of 3 m and 4 m and a silty sand with numerous shell fragments but enough clay to provide an effective matrix was present between depths of 4 m and 5 m. A clean sand layer occurred between depths of 5 m and 6 m, and below 6 m, the soil...
consisted of high plasticity clay similar to the soil in the upper 3 m, but with greater strength due to higher consolidation stress.

Fig. 5 illustrates the site investigation results. The results of unconfined compression tests are consistently lower than those of the vane and were not relied upon by Matlock [20] when establishing the shear strength profile. Fig. 5 illustrates the strength profile adopted by the current back-analysis, which is consistent with those of Matlock [20] and Jeanjean et al. [11] despite some minor simplifications near the surface (Fig. 5). The current back-analysis neglects the sandy layers between 13 and 20 feet (4–6 m) below the ground surface and assumes a continuous undrained shear strength profile within this depth interval, where significant scatter of vane results is seen. The undrained shear strength profile is taken to be representative of strength measured in DSS tests. It remains constant at 13 kPa from ground surface to 2 m depth and then increases linearly with depth at a gradient of 1.54 kPa/m. The submerged unit weight of the soil was not reported and is estimated to be 6 kN/m³. The plasticity index (I_p) for the surface plastic layer is between 50–70%, which is similar to typical GoM material.

The over-consolidation ratio (OCR) of the soil at the test site is estimated using the SHANSEP method [15]:

\[ s_u = \left( \frac{s_u}{\sigma'_{NC}} \right)_{OCR} \]  

(1)

Assuming a \( s_u/\sigma'_{NC} \) ratio of 0.25 and \( m = 0.8 \) based on typical values for Gulf of Mexico clay [16], the OCR is estimated using Eq. (1) together with the \( s_u \) profile recommended for back-analysis as illustrated in Fig. 5. It can be seen that and the OCR decreases rapidly with depth from around 20 at 1 m below excavated ground surface to 2 at 10 m depth. A simplified stepwise OCR profile, as illustrated in Fig. 5 is used in the back-analyses. This point will be further discussed.

For the back-analyses, the pile-soil interface roughness factor (α) was estimated using the method recommended in API RP 2GEO [5] for calculating the axial shaft friction of driven piles in clay:

\[ \alpha = 0.5 \left( \frac{\sigma'_u}{\sigma'_c} \right)_m^{0.5} \]  

for \( \sigma'_u/\sigma'_c \leq 1.0 \)

\[ \alpha = 0.5 \left( \frac{\sigma'_u}{\sigma'_c} \right)_m^{0.25} \]  

for \( \sigma'_u/\sigma'_c > 1.0 \)

(2)

The value of \( \alpha \) is between 0 and 1.0. Based on the above equation, an average interface roughness factor of 0.6 is estimated and was used in the back-analysis.

According to the empirical guidance from Jeanjean et al. [11], a gap is expected to open on the back side of the pile during lateral loading and indeed was observed during cyclic testing (gap formation was not documented for the static tests). Presence of a gap is therefore assumed in the back-analyses. The effect of shear strength anisotropy on the ultimate lateral bearing capacity for the wedge failure was accounted for according to the method suggested in Jeanjean et al. [11]. A typical anisotropy ratio \( (s_{uv}/s_{ud}) \) (triaxial extension strength over DSS strength) for GoM clays of 0.9 was assumed.

### 3.2.3. Monotonic and cyclic stress-strain behaviour

The back-analyses assume that the monotonic and the cyclic stress-strain behaviours of the Sabine River clay are similar to those of GoM clays. Zhang et al. [28] presented the DSS monotonic and the cyclic properties of normally consolidated GoM clay (i.e. OCR = 1) based on
an extensive database from ten sites in the GoM. Reference is made to Zhang et al. [28] for the details. For completeness, Fig. 6 presents the cyclic strain contour diagrams for normally consolidated GoM clays under DSS shearing mode. Each point on the contour diagram represents the average and cyclic shear strains that are developed on a DSS soil element when it is cyclically loaded under the corresponding average and cyclic shear stresses for the specified number of cycles.

3.2.3.1. Correction for OCR effect on the stress-strain behaviour. It is well understood that higher OCR leads to more ductile stress-strain response due to dilative behaviour of high OCR clays, which requires larger strains to mobilise its strength. This is illustrated by for example triaxial tests of reconstituted kaolin [23] and DSS tests of Drammen clay [3] on samples consolidated to different OCRs. Jeanjean et al. [11] reports a database of 537 DSS stress-strain curves that was compiled from tests on samples from 5 offshore regions which also reveals a clear trend, as illustrated in Fig. 7.

As illustrated by Fig. 5, the soil at the Sabine River is over-consolidated, although the OCR reduces rapidly with depth. However, due to the small diameter of the pile tested (0.324 m), the effect of OCR should be taken into account when back-analysing the field test results. Since the monotonic and cyclic properties of over-consolidated GoM clay are not available, the OCR effect is accounted for in an empirical manner here. Fig. 8 shows the ratio of normalised secant shear modulus value at 50% strength mobilisation ($G_{50}/s_u$) measured in DSS test between over-consolidated specimen and normally consolidated

![Fig. 6. Cyclic strain contour diagrams for normally consolidated GoM clay under DSS shearing mode.](image-url)
specimen for several different clayey soils as well as the trend suggested by the Jeanjean et al. [11] database (the data points shown in the figure were evaluated based on a parameter “a” following the trend line shown in Fig. 7, an assumed constant $G_{\text{max}}/s_u=500$, and $\gamma_{pf}=0.139$ for all OCRs). The $G_{50}/s_{UD}$ ratio clearly decreases with increase of OCR. All the data appears to agree reasonably well, despite that the trend suggested by the Jeanjean et al. [11] database plots slightly higher, which is believed due to the assumption of constant $G_{\text{max}}/s_u$ and $\gamma_{pf}$ values, resulting in underestimation of the stiffness for normally consolidated soils and over-estimation of the stiffness for over-consolidated soils. To account for the effect of OCR, the $G_{50}/s_{UD}$ ratio between over-consolidated soil and normally consolidated soil implied by the best-fit line drawn in Fig. 8 is used to scale the strain values in the monotonic stress-strain response and in the cyclic strain contour diagrams to derive soil responses for over-consolidated soils. It should be noted that this is an approximate way to account for the OCR effect. At very small strains, the impact of OCR is less. The correction applied hereby may thus result in too soft initial response at low mobilisation levels. Fig. 9 presents the monotonic stress-strain curves for different OCRs scaled from that for normally consolidated GoM clay and corresponding p-y curves that were used in the back-analysis.

3.2.4. Back analysis of monotonic test

The normalised monotonic p-y curves presented in Fig. 9 were used. Two back-analyses were performed: analysis no.1 uses the undrained shear strength profile as illustrated in Fig. 5; and analysis no. 2 with a factor of 1.3 applied to the undrained shear strength profile. The 1.3 factor accounts for the rate effect due to the difference in rate of loading between the DSS tests and the pile load test, as discussed below. Fig. 10 presents the results of the back-analyses in comparison with the measured response. From the inserted plot it can be seen that the back-analysis without considering the strain rate effect considerably over-estimates the pile head deflection (measured 0.3 m above test ground surface). On the other hand, the back-analysis with rate effect...
yields a much improved match with the measured response. This comparison raises an important aspect that need to be considered between laboratory soil element test and field or model pile tests in general. The laboratory monotonic DSS test is typically carried out at a constant shear strain rate of about 5% per hour. Consider a failure strain of 15% for the GoM soil, this means 3 h to failure. In the field/model testing, such extended loading time is generally not used. With regard to the Sabine River test, the pile head load was applied in 5 increments. The exact duration of each load increment is unknown, and the factor of 1.3 is thus uncertain. However, considerable rate effect relative to the laboratory strain rate is expected. This may partially explain why the back-analysis without the rate effect predicts softer response than measured. The negligence of the sandy layers between 4–6 m may have also contributed to the difference.

Fig. 10 also presents a comparison of the lateral deflection and bending moment profiles along the pile between the back-analysis and the measured response for the free head monotonic loading test at five different pile head load levels. The results of back-analysis with rate effect are presented. A reasonably good match is demonstrated.

Table 1

| Parcel | No. of cycles | Min load, kN | Max load, kN | Ave. load, kN | Cyc. load, kN |
|--------|--------------|-------------|-------------|--------------|--------------|
| 1      | 400          | −8.9        | 17.8        | 4.45         | 13.35        |
| 2      | 200          | −8.9        | 35.6        | 13.35        | 22.25        |
| 3      | 200          | −8.9        | 53.4        | 22.25        | 31.15        |
| 4      | 200          | −8.9        | 60          | 25.55        | 34.45        |

3.2.5. Back analysis of cyclic test

Table 1 summaries the load history of the Sabine River free head cyclic lateral load test. The load history consists of four load parcels. Within each parcel, the cyclic loading remains constant. The load level increases with the parcel number. Except Parcel 1, all the remaining three parcels have 200 load cycles. The period for each load cycle is 20 s.

Fig. 11 presents the results of the back-analysis, including the evolution of sectional bending moment and the lateral deflection along the
pile with cyclic loading. Test results, where available, are presented for comparison. It should be noted that the test results are based on readings of peak strain gauge values during continuous cyclic loading. The results along the depth do not correspond to a given moment, but for a given period, as indicated by the legend. The change of the values during the time period is assumed to be small as the readings were typically taken when cyclic degradation had stabilised in each parcel. The agreement between the test results and the back-analyses is very good for the first two load parcels. However, from parcel 3, the model predicts stiffer response than the behaviour actually observed. In parcel 4, the model predicts a pile response that becomes stabilised and exhibits limited degradation with cyclic loading. In comparison, the field test suggests significant degradation in stiffness and large increase in bending moment. One important aspect that is believed to contribute to the large difference between back-analysis and test observation in parcel 3 and parcel 4 is the progressively developed permanent displacement of soil away from the pile. Under the lateral loading, the soil in front of the pile is pushed away and a cavity is formed behind the pile due to permanent soil deformation. Although the cavity is only measured in the end of the cyclic test, it is postulated that the cavity grows in size and depth as the cyclic loading progresses. During a load cycle, the pile feels no soil resistance until it is pushed far enough to close up the gap again. This causes an apparent “degradation” of the soil-pile interaction stiffness. However, this phenomenon is not captured by the current model, which is fundamentally based on a flow-around soil mechanism. Although the current model accounts for tension gap opening partially by reducing the ultimate strength of the p-y curve, it assumes that soil follows the movement of the pile, and the decrease of the soil-pile interaction stiffness predicted by the model is entirely due to the degradation of the soil.

However, it is important to reflect on the significance of the above discrepancy between model prediction and field observation for the practical design of offshore piles for oil and gas platforms. There are two points to be noted:

1) In the cyclic pile tests at Sabine River, four parcels of constant amplitude cyclic loading were consecutively applied to the pile head. The cyclic load amplitude increased consecutively. In the largest load parcel, the peak horizontal load would have resulted in more than 10% pile deflection at ground surface if the load had been applied monotonically. This represents an extremely high load level. 200 cycles were applied in each load parcel, except the first one, where 400 cycles were applied. This differs significantly from the actual load history encountered by pile foundations supporting offshore structures. Zhang et al. [31] suggests that the equivalent number of cycles along a pile foundation supporting a jacket structure in Gulf of Mexico and the North Sea is typically less than 25.

2) A mudmat is typically placed on the soil surface, enclosing a pile or a pile group at each corner of the legs supporting a jacket structure. The mudmats are designed to support the jacket structure prior to piling, but it also acts as a seal and cuts off the seepage path for water getting into the pile-soil interface during cyclic loading. The soil is then forced to adhere to the movement of the pile. The gap-ping mechanism, which led to the “apparent degradation” of soil-pile interaction stiffness in the Sabine River test, is thus considered unlikely to occur in practice, even for piles in stiff clay.

In summary, the limitations of the model in predicting the Sabine River cyclic test results for the very large displacement levels and number of cycles is not deemed critical for the design of oil and gas platforms.
3.3. Zakeri et al. [25] centrifuge model testing

3.3.1. Geometry and instrumentation

The centrifuge tests were performed at 55.35g. The model pile had a diameter of 17.4 mm and a wall thickness of 0.92 mm and was made of grade 4140 steel. It was equipped with 18 levels of strain gauges to measure the bending moment profile along the pile. Due to the epoxy coating on the strain gauges, the diameter of the pile was slightly increased. In prototype scale, the pile had an outer diameter of 0.963 m, an inner diameter of 0.879 m and a wall thickness of 42 mm. All the results are reported in prototype scale below, unless otherwise stated.

The model pile was installed through a predrilled hole at 1g upon completion of lab floor consolidation of the soil sample. The soil was further consolidated at testing g level in the centrifuge. A final pile embedment depth of 25.74 m was achieved. During the pile tests, the displacement-controlled loading was applied through a pin connection located at 4.76 m above the ground surface.

3.3.2. Soil condition

The centrifuge experiments were carried out in lightly over-consolidated Kaolin clay. Fig. 12 illustrates two mini T-bar test results and interpreted undrained shear strength profile, using a $N_{T-bar}$ factor of 10.5. Shallow correction presented by White et al. [24] was applied in interpretation of the strength in the upper 1.1 m (20 mm in model scale, which corresponds to 2.5 T-bar diameters in the centrifuge). According to Low et al. [17], $N_{T-bar} = 10.5$ would for typical natural clays give the triaxial compression strength. Therefore, the strength profile presented in Fig. 12 is taken to be the triaxial compression strength. Andersen et al. [2] reports $s_{ud}/s_{uc} = 0.9$ for Kaolin clay. This anisotropy ratio was assumed to derive the DSS strength for the back-analysis presented below.

Due to the very low undrained shear strength at mudline, no tension gap was observed in the centrifuge tests. The back-analyses presented below therefore assumed no gapping. Furthermore, a fully rough pile-soil interface roughness was considered.

3.3.3. Stress-strain responses under monotonic and cyclic shear stresses

There were no cyclic soil element tests carried out on the Kaolin clay used in the centrifuge experiments. The Kaolin clay cyclic properties used in this back-analysis were based on a collaborative study between the University of Western Australia (UWA) and the Norwegian Geotechnical Institute (NGI), as reported in Carotenuto et al. [7]. All the DSS tests were performed at NGI on normally consolidated Kaolin, prepared from the PRESTIGE-NY Kaolin powder, supplied by Sibelco Australia. This Kaolin is widely used for centrifuge model testing at UWA and hence is referred as UWA Kaolin clay hereafter. The plasticity index ($I_p$) of the UWA Kaolin clay is measured to be 28%.

The monotonic DSS stress-strain response of kaolin reported by Jeanjean et al. [11] was complemented by five additional monotonic tests carried out at NGI on UWA kaolin to augment the database as properties of the kaolin clay can vary between suppliers.

3.3.3.1. Monotonic stress-strain behaviour

Five monotonic DSS tests were carried out on normally consolidated UWA Kaolin with a shear strain rate of 4.7% per hour. The results were very repeatable. Fig. 13 presents the representative normalised stress-strain curves of the UWA Kaolin and the p-y curve constructed using an interface factor $\alpha = 1.0$, which was used in the back-analysis below. The initial stiffness of the normally consolidated UWA kaolin was estimated from the stiffness degradation curves measured in the five monotonic DSS tests by extrapolating to small strains. A $G_{max}/s_{ud} = 500$ is estimated.

![Fig. 12. Undrained triaxial compression shear strength profile of Zakeri et al. [25] centrifuge tests.](image-url)
3.3.3.2. Cyclic contour diagrams. In total 11 cyclic DSS tests were carried out on normally consolidated UWA kaolin to develop the cyclic interaction diagrams. These tests cover different combinations of normalised average and cyclic shear stresses. Further details on those cyclic DSS tests and the cyclic contour diagrams can be found in Carotenuto et al. [7]. Compared with Drammen clay [1], the UWA kaolin degrades faster with number of load cycles.

3.3.4. Back-analysis of monotonic test

The monotonic test was performed displacement controlled at a rate of circa 8% pile diameter per second, which is approximately 3 orders of magnitude higher than a typical laboratory DSS test. To account for the increase in shearing rate between the DSS test and the pile test, the shear strength was increased by 25% in the back analysis. This correction is in the low range of the rate effect data base presented by Lunne and Andersen [18].

Fig. 14 presents the measured and back-analysed lateral deflection and bending moment profile with depth at three different pile head load levels as well as the pile head load-displacement response for the monotonic push-over test, with good agreement.

3.3.5. Back-analysis of cyclic tests

Two cyclic pile tests under harmonic displacement cycles are back-analysed. The cyclic displacement motions were applied to the pile head, and the horizontal force exerted to the pile head was measured. In each test, a series of motions with different displacement amplitudes were applied consecutively, with three months, in prototype units, waiting period in-between two cyclic motions. Each displacement motion consisted of 1000 cycles. Table 2 summaries the applied displacement motions in those two tests. In Test C2, the displacement is symmetric (i.e. two way cycling) and the cyclic amplitude increases with motion number, except the last one. In the back-analysis presented below, each motion is treated as an independent test, i.e. assuming the previous loading history is totally erased due to higher load level applied in the current motion. Apparently, this does not hold for Motion M2b, which was therefore not back-analysed. In Test C3, M1 is a two way symmetric cycling. However, in motion 2–5, an average displacement component (offset) is introduced. Since the total displacement amplitude in motion 4 is reduced from motion 3, only the first three motions in this test were back-analysed, assuming each motion as an independent cyclic test.

Fig. 14. Back-analysis of the monotonic test (pile head displacement measured at the load application point).
3.4. SOLCYP centrifuge model testing

Khemakhem [14] reports a comprehensive set of centrifuge model tests of piles in Kaolin clay under monotonic and cyclic lateral loading. Those tests formed part of the SOLCYP project, which is summarized in Puech and Garnier [22]. Selected monotonic and cyclic tests carried out in slightly over-consolidated Kaolin were back-analysed using the currently proposed model. The details of the tests and back-analyses are presented below.

3.4.1. Geometry and instrumentation

The model tests were carried out at the IFSTTAR centrifuge facility. All the tests were run at 50 g. Table 3 summarizes the geometries of the model pile and dimensions used in back-analysis.

In the discussions and back analyses presented below, unless otherwise stated, all dimensions refer to prototype scale. The model pile is instrumented with 21 levels of strain gauges to measure the bending moment along the pile. The gauges are evenly spaced vertically, 0.75 m (prototype scale) apart. The pile is loaded 2 m above the mudline, where the applied force and induced lateral displacement are measured.

3.4.2. Soil conditions

Two types of soil conditions were tested by Khemakhem [14], namely saturated, slightly over-consolidated clay and unsaturated, heavily over-consolidated clay. The back-analyses reported herein focus on tests carried out in the saturated, lightly over-consolidated clay. The tests were carried out on Kaolin clay. The soil sample was prepared from Kaolin slurry mixed under vacuum to 90% water content, consolidated at 1 g under a hydraulic press. To achieve the desired sample height, the sample was prepared in three layers. Before the pile tests, the sample was reconsolidated under 50 g in-flight. The undrained shear strength ($s_u$) was established from in-flight cone penetration tests using the empirical correlation presented by Garnier [9].

$$s_u = q_c/18.5 \tag{3}$$

where $q_c$ is the measured cone resistance.

It is unclear which shear mode the correlated shear strength corresponds to and in the back-analyses, it is assumed to represent an average strength, which is typically similar to the DSS strength. Considerable variation within a soil sample and across different soil samples was revealed by the in-flight CPT tests, as illustrated in Fig. 17. Khemakhem [14] attributed the variation to the inadequate pressure control of the hydraulic press that was used to prepare the soil samples at 1 g. Based on the results measured in four samples, low and high estimate profiles are drawn. In the Figure, the representative profile suggested by Khemakhem [14] is also illustrated for comparison. In the back-analysis below, except for the chosen monotonic test, it was unfortunately not possible to identify the test specific shear strength
All the back-analyses presented below were performed using a representative profile suggested by Khemakhem [14]. However, the variation of the strength profile should be borne in mind when evaluating the results of the back-analyses. Fig. 17 also presents the estimated over-consolidation ratio (OCR) based on the stress history applied to soil during sample preparation.

For the back-analyses, a fully rough soil-pile interface roughness factor was assumed. In addition, the interface is allowed to gap freely, which is consistent with the observation in the tests.

The soil response of the Kaolin clay under monotonic and cyclic loading is already summarized in Section 3.3. However, those tests were for normally consolidated Kaolin. Based on Fig. 17, the SOLCYP soil samples have OCR greater than 1. As discussed previously, a soil with an OCR greater than one generally exhibits more ductile response than normally consolidated soil under monotonic loading, and more rapid degradation under cyclic loading. In the back analyses, the OCR effect is accounted for in an approximate manner due to lack of tests data for kaolin at OCR greater than one. Based on the trend illustrated...
in Fig. 8, correction factors were evaluated. For the depth interval (0–6.6 m), an average OCR = 4 is assumed and an OCR = 2 is assumed for deeper soils. For OCR = 4, the $G_{50}/s_{uD}$ ratio is reduced to approximate 40% of that for OCR = 1, which implies a stiffness reduction factor of 2.5. For OCR = 2, the $G_{50}/s_{uD}$ ratio is reduced to approximate 70% of that for OCR = 1, which implies a stiffness reduction factor of 1.4. These stiffness reduction factors were applied to scale up the strains in the cyclic contour diagrams (for both the average and the cyclic strain components). The effect of OCR on the normalised monotonic p-y curve is illustrated in Fig. 17.

### Table 3
Summary of pile geometry in model scale and prototype scale.

| Parameter                | Model scale | Prototype scale (used in back analyses) |
|--------------------------|-------------|----------------------------------------|
| Total pile length       | 360 mm      | 18 m                                   |
| Penetrated length       | 320 mm      | 16 m                                   |
| Diameter                | 18 mm       | 0.954 m$^*$                           |
| E, GPa (Aluminium)      | 74          | 74                                     |
| Wall thickness           | 1 mm        | 40 mm$^*$                              |

$^*$ The pile diameter and the wall thickness do not scale proportionally to the g level as the coating on the strain gauges enlarge the pile diameter by 6% [14].

#### 3.4.3. Pile installation and loading

The model pile was installed at 1g. A slightly oversized hole was first created by a manually operated auger. The test pile is then placed into the predrilled hole. The small clearance between the pile shaft and the soil at the surface is closed by hand. The clearance below the mudline is assumed to be closed by self-weight of the soil when it is ramped up and reconsolidated under 50 g.

The pile head load is applied 2 m above the mudline. The monotonic tests were run in displacement-controlled mode at a constant velocity of 0.4 mm/s (model scale) or 20 mm/s at prototype scale. At this displacement rate, 10% pile diameter is reached within 4.8 s. This is approximately three orders of magnitude faster than a standard monotonic DSS test. Significant rate effect is expected. This point will be further discussed in the result section.

The cyclic tests were run in load-controlled mode, where sinusoidal load history was applied to the pile head. For tests run with a non-zero average horizontal load, the loading consists of two phases:

- **Phase 1**: application of the average load. This was applied at a speed of 0.02 kN/s (model scale) or 50 kN/s in prototype scale. Again, this is an extremely fast loading speed, compared to a monotonic pile capacity of 220 kN at 10% of a diameter pile head deflection. While this average load is held during the cyclic pile testing, pile head deflection due to the average loading is expected to increase with time due to creep. This aspect will be further discussed below.
- **Phase 2**: application of the cyclic horizontal load. All the tests were run with a frequency of 0.25 Hz, i.e. a loading period of 4 s.

#### 3.4.4. Back-analysis of monotonic test

One monotonic lateral pile load test was back analysed. For this selected test, the soil strength profile is reported in Khemakhem [14], which corresponds to the “Representative profile Khemakhem [14]” shown in Fig. 17. As mentioned above, the shear strain rate experienced by the soil during the monotonic pile test far exceeded the strain rate applied in the monotonic DSS tests. In the back analysis, a 25% increase in mobilised soil strength is assumed to account for the rate effect. This rate effect correction is in the low range of the rate effect data base

![Fig. 17. Low and high estimate undrained shear strength, OCR versus depth and monotonic p-y curves for different OCR values.](image-url)
Fig. 18. Comparison of bending moment profile for monotonic test SOLCYP05S1ins.

presented by Lunne and Andersen [18]. Fig. 18 presents the comparison of the measured pile head load-displacement curve against the back-analyses, with and without consideration of the rate effect and shows that the analysis without considering the rate effect under-predicts the system stiffness. The match is much improved when the rate effect is taken into consideration. Fig. 18 also illustrates the comparison of the bending moment profile along the pile between the physical measurements and the back-analysis (with consideration of the rate effect) at three different load levels. Again, a good match is demonstrated.

3.4.5. Back-analyses of cyclic tests

Two cyclic pile tests reported by Khemakhem [14] were chosen for back-analysis. The details of the two tests are summarized in Table 4.

Table 4

| Test name | Average load, kN | Cyclic load, kN | No. of cycles |
|-----------|-----------------|----------------|--------------|
| C09S1ins  | 150             | 200            | 40           |
| C10S1ins  | 150             | 50             | 1000         |

The two tests have the same average lateral load level (150 kN), but different cyclic amplitudes. Test C09S1ins has a large cyclic amplitude and the load direction is reversed during each cycle, while test C10S1ins has a relatively small cyclic amplitude and the lateral load does not reverse direction during cycling.

Figs. 19 and 20 present the results of back-analysis for test C09S1ins. Fig. 19 compares back-analysed and the measured the bending moment profile along the pile length in the 10th cycle. A reasonably good match is demonstrated, although the back-analysis predicts slightly higher bending moment. It is noted that near the ground surface, the back-analysis already suggests slightly higher bending moment, which may indicate that the applied load in the physical test is possibly smaller than 350 kN. Fig. 20 compares the evolution of pile head deflection and maximum bending moment along the pile with the number of applied load cycles. The back-analysis predicts a similar trend to the experimental observation. However, towards the end of the test, the experiment appears to exhibit accelerated increase in bending moment and pile head deflection, indicating imminent failure. The back-analysis however predicts more steady development of pile head deformations. In the figure, the back-analysis by Khemakhem is also presented. In general, the current back-analysis performs better or similarly.

The back-analyses of the two cyclic tests illustrates that the cyclic model generally captures the trend revealed by the centrifuge tests, although some discrepancies are noted. As discussed in Section 3.4.2, uncertainties exist with the exact undrained shear strength profiles in the cyclic tests. Furthermore, the effect of tension gapping, which causes an apparent degradation of the soil-pile interaction stiffness due to permanent soil displacement, as discussed in Section 3.2.5, is also likely to have contributed to the difference between model prediction and the test measurements.
4. Concluding remarks

This paper presented verification of a framework for analysing the pile response under cyclic lateral loading. The framework is based on fundamental soil performance measured at soil element level. It allows for consideration of site-specific cyclic soil properties, including effects of over-consolidation ratio, rate of loading and strength anisotropy, as well as interface roughness, gapping and project specific cyclic loading characteristics into the pile foundation design. This is a step-change improvement from current codes and standards recommendations which are based on a series of tests on a single pile at a single site (the...
Sabine River tests). The framework was used in the back-analyses of four series of model/centrifuge pile tests (although only three test series were reported in this paper) which demonstrated its ability to capture the essential behaviour of pile foundations under cyclic lateral loading and its potential for application in the design of long slender piles for offshore platforms.

CRediT authorship contribution statement

Youhu Zhang: Conceptualization, Methodology, Software, Validation, Investigation, Writing - original draft. Knut H. Andersen: Conceptualization, Resources, Investigation, Writing - review & editing. Philippe Jeanjean: Conceptualization, Resources, Investigation, Writing - review & editing.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Supplementary materials

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