Vortex Imaging in the $\pi$-Band of Magnesium Diboride

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We report scanning tunneling spectroscopy imaging of the vortex lattice in single crystalline MgB$_2$. By tunneling parallel to the $c$-axis, a single superconducting gap ($\Delta = 2.2$ meV) associated with the $\pi$-band is observed. The vortices in the $\pi$-band have a large core size compared to estimates based on $H_{c2}$, and show an absence of localized states in the core. Furthermore, superconductivity between the vortices is rapidly suppressed by an applied field. These results suggest that superconductivity in the $\pi$-band is, at least partially, induced by the intrinsically superconducting $\sigma$-band.

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Superconductivity in magnesium diboride (MgB$_2$) with a remarkably high $T_c = 39$ K was recently reported by Nagamatsu et al. \cite{1}. Since then, great attention has been directed towards understanding the detailed nature of superconductivity in this material, in an particular whether this is a one- or two-gap superconductor. Two-gap superconductivity was predicted theoretically \cite{2,3}, and is now supported by an increasing number of experimental reports \cite{4,5,6,7,8,9,10,11,12,13,14,15}. Two-gap or two-band superconductivity was first studied in the fifties \cite{16}, and has now found renewed relevance in MgB$_2$. In addition, and contrary to many materials or alloys studied earlier, the two bands in MgB$_2$ have roughly equal filling factor, opening the possibility for interesting new phenomena. However, the exact microscopic details are still largely unexplored. An ideal way to address this issue is by local spectroscopic investigations of the mixed state, which has become possible with the recent availability of high quality MgB$_2$ single crystals.

In this Letter we report on scanning tunneling spectroscopy (STS) measurements on single crystal MgB$_2$, including the first vortex imaging in this material. Tunneling parallel to the $c$-axis, we are able to selectively measure only the $\pi$-band \cite{17,18}, in which the vortices are found to have a number of remarkable properties: An absence of localized states, a very large vortex core size compared to the estimate based on $H_{c2}$, and a strong core overlap.

The STS experiments were performed using a home built scanning tunneling microscope (STM) installed in a $^3$He, ultra high vacuum cryostat holding a 14 T magnet \cite{19}. The measurements were done on the surface of an as grown single crystal, using electrochemically etched iridium tips. Single crystals of MgB$_2$ were grown using a high pressure method described elsewhere \cite{20}, yielding platelike samples with the surface normal parallel to the crystalline $c$-axis. The surface of the crystals are roughly $0.25 \times 0.25$ mm$^2$, and the thickness of the order of microns. The critical temperature is typically $T_c \approx 38 - 39$ K, with a sharp transition, $\Delta T_c = 0.5$ K, measured by SQUID magnetometry \cite{17}. The STS experiments were done with both the tunneling direction and the applied magnetic field parallel to the $c$-axis, and the differential conductivity measured using a standard AC lock-in technique. In this configuration the upper critical field extrapolates to $H_{c2}(T = 0K) = 3.1$ T \cite{17}. Using the Ginzburg-Landau (GL) expression for $H_{c2} = \phi_0/(2\pi c^2)$, where $\phi_0 = h/2e$ is the flux quantum, yields a coherence length, $\xi_{GL} = 10$ nm. An estimate of the mean free path, based on the measured residual resistivity \cite{21} and specific heat \cite{22}, and the calculated Fermi velocity \cite{23}, gives $l \approx 50 - 100$ nm, indicating that the samples are in the clean limit.

We will first focus on the zero-field electronic spectrum of MgB$_2$. The observation of a single or double gaps depends on the orientation of the sample, as shown by Iavarone et al., who investigated a number of single grains with different, but unknown absolute orientations \cite{24}. Here we report the first STS measurements on a MgB$_2$ single crystal, which allow a correlation between the tunneling direction and the observed gap(s). In Fig. 1 we show a superconducting spectrum obtained at a temperature of 320 mK. This is an average of 40 spectra obtained along a 100 nm path, which shows perfect homogeneity. One observes a single gap with coherence peaks at ±2.5 meV, and additional weak shoulders at ±6 meV, as indicated by the arrows. In addition, the flat region around the Fermi energy proves the absence of nodes in the gap, and hence that MgB$_2$ is a $s$-wave superconductor. The very low zero bias conductance indicates a high quality tunnel junction and a low noise level. True vacuum tunneling conditions were assured by varying the tunnel resistance, $R_t$, and verifying that the spectra normalized to the conductance outside the superconducting gap collapse on a single curve. The spectrum can be fitted by the BCS expression for the density of states (DOS), including a finite quasiparticle lifetime, $\Gamma$ \cite{25}, and an experimental broadening. The result of the fit is shown in Fig. 1 and yields a superconducting gap, $\Delta = 2.2$ meV. We have studied the temperature depen-
depends on the tunneling direction. The tunneling matrix element is different for the two bands, and involves orbitals and is three-dimensional [2, 3, 20]. The tunneling states of the boron two distinct sheets: One is derived from \(\sigma\) of how tunneling along different directions is coupled to superconductivity and found excellent evidence of the superconducting gap and normalized this to the conductance at the coherence peak. Low values of the normalized conductance correspond to superconducting areas, and high values to the vortex cores. The low field is equivalent to a separation, \(d = 220 \text{ nm} \gg \xi\). The vortices can therefore be considered as isolated from each other. Such isolated vortices are expected to contain localized quasiparticle states, which should show up as a zero bias conductance (ZBC) peak at the vortex centre [21], provided that the sample is sufficiently clean to prevent these to be smeared out by scattering. We have measured the evolution of the spectra at a large number of positions along a trace across the vortex core as shown in Fig. 2c. Contrary to expectations, we find that the normalized ZBC increases to one with no indication of any localized states. Instead, the spectra in the centre of the vortex are absolutely flat, with no excess spectral weight at or close to zero bias. This absence of localized states is striking, considering that \(l = 5 - 10 \times \xi_{GL}\). However, as we will show below, the coherence length in the \(\pi\)-band is approximately 50 nm. This is much larger than the estimate based on \(H_{c2}\), and equal to only one to two times the mean free path. Nonetheless, systematic studies of Nb\(_{1-x}\)Ta\(_x\)Se\(_2\) with \(x = 0 - 0.2\), showed that even for \(\xi/l \approx 1\) some excess weight close to zero bias was observed [22]. In parallel to STS imaging, STM topographic images were recorded (not shown), which revealed a flat surface with a RMS roughness of 6 Å over the whole image area.

Before analyzing the vortex profile in detail, we will consider the situation at higher fields. In Fig. 2b we show the STS image of the hexagonal vortex lattice observed at 0.2 T. We notice that the normalized ZBC between the vortices, is now enhanced with respect to the value far from the single vortex at 0.05 T. This increase of the “bulk” ZBC is unusual at such a modest field, only about 7% of \(H_{c2}\). To elucidate this behaviour, “bulk” spectra for fields between zero and 0.5 T are shown in Fig. 2d. It is clear that even modest fields rapidly suppress superconductivity in the region between the vortices. This is seen both by an increase of the ZBC and by a suppression of the coherence peaks outside the vortex cores, which one would only expect for fields close to \(H_{c2}\), corresponding to a significant core overlap. This is consistent with earlier point contact spectroscopy measurements [3], with the addition that we resolve the local behaviour on a microscopic scale.

The vortex spacing is determined by the applied field and the flux quantization, and in the case of a hexagonal vortex lattice it is \(d = (2/\sqrt{3} \phi_0/H)^{1/2}\). The magnetic fields were applied at 2 K, and the system allowed to stabilize for at least a few hours. After this time no vortex motion was observed, indicating a fast relaxation and hence low vortex pinning in the crystal.

In Fig. 2a we show a STS image of a single vortex induced by a field of 0.05 T. The image was obtained by measuring the differential conductance at zero bias and normalizing this to the conductance at the coherence peak. Low values of the normalized conductance correspond to superconducting areas, and high values to the vortex cores. The low field is equivalent to a separation, \(d = 220 \text{ nm} \gg \xi\). The vortices can therefore be considered as isolated from each other. Such isolated vortices are expected to contain localized quasiparticle states, which should show up as a zero bias conductance (ZBC) peak at the vortex centre [21], provided that the sample is sufficiently clean to prevent these to be smeared out by scattering. We have measured the evolution of the spectra at a large number of positions along a trace across the vortex core as shown in Fig. 2c. Contrary to expectations, we find that the normalized ZBC increases to one with no indication of any localized states. Instead, the spectra in the centre of the vortex are absolutely flat, with no excess spectral weight at or close to zero bias. This absence of localized states is striking, considering that \(l = 5 - 10 \times \xi_{GL}\). However, as we will show below, the coherence length in the \(\pi\)-band is approximately 50 nm. This is much larger than the estimate based on \(H_{c2}\), and equal to only one to two times the mean free path. Nonetheless, systematic studies of Nb\(_{1-x}\)Ta\(_x\)Se\(_2\) with \(x = 0 - 0.2\), showed that even for \(\xi/l \approx 1\) some excess weight close to zero bias was observed [22]. In parallel to STS imaging, STM topographic images were recorded (not shown), which revealed a flat surface with a RMS roughness of 6 Å over the whole image area.

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We now return to the single vortex measurement. In Fig. 3a, we have plotted the normalized ZBC, $\sigma'(x,0)$, for the vortex trace measured at 0.05 T. It is immediately clear that the spatial extension of the vortex core is much larger than the 10 nm estimated from $H_{c2}$. Somewhat surprisingly, we find that the ZBC profile can be fitted by one minus the GL expression for the superconducting order parameter:

$$\sigma'(x,0) = \sigma'_0 + (1 - \sigma'_0) \times (1 - \tanh x/\xi), \quad (1)$$

where $\sigma'_0 = 0.068$ is the normalized ZBC measured in zero field. The fit, shown in Fig. 3a, yields a coherence length, $\xi = \xi_n = 49.6 \pm 0.9$ nm. Using the GL expression to calculate the upper critical field with this value of the coherence length, yields $H'_{c2} = 0.13$ T. At 0.2 T we hence find ourselves in the bizarre situation of imaging the vortex lattice above the nominal $H'_{c2}$. Additional vortex lattice imaging has been performed as high as 0.5 T.
This apparent paradox can be reconciled if one assumes that superconductivity in the $\pi$-band is induced by the $\sigma$-band, either by interband scattering, or Cooper pair tunneling [13, 23]. This means that isolated the $\sigma$-band would either be non-superconducting or have a very low upper critical field. Consequently the observed behaviour reflects the state in the $\sigma$-band by an interband proximity effect, along the lines of recent theoretical work [23]. The vanishing of $\Delta_{\pi}(T)$ at the bulk $T_c$ further supports this conclusion. Finally, it is also consistent with estimates of the coherence lengths, using the BCS expression $\xi_0 = h\nu_F/(\pi\Delta(0))$ and considering each band separately. Taking the calculated average Fermi velocity in the $ab$-plane for the $\pi$-band, $v_{\pi}^F = 5.35 \times 10^7$ m/s [14], and the measured gap value $\Delta_{\pi} = 2.2$ meV we get $\xi_0^\pi = 51$ nm, in excellent agreement with $\xi_\pi$ obtained from the vortex profile. A similar analysis for the $\sigma$-band, using $v_{\sigma}^F = 4.4 \times 10^7$ m/s [13] and $\Delta_{\sigma} = 7.1$ meV [12] yields $\xi_0^\sigma = 13$ nm. This agrees with the coherence length obtained from $H_{c2}$, and reinforces the conclusion that it is mainly the $\sigma$-band which is responsible for superconductivity in MgB$_2$, and thus determines the macroscopic parameters $T_c$ and $H_{c2}$.

As described above, it is the transfer from the $\sigma$-band that makes superconductivity in the $\pi$-band possible, despite a strong vortex core overlap already at very low magnetic fields. Constructing a simple model for the core overlap in the $\pi$-band by

$$\sigma'(r, 0) = \sigma_0' + (1 - \sigma_0') \times \left(1 - \Pi, \tanh \frac{|r - r_i|}{\xi_\pi}\right),$$  

(2)

where $r_i$ are the vortex positions for a hexagonal lattice with a density corresponding to the applied field, we can calculate the ZBC at any position in the vortex lattice unit cell. In Fig. 3b we compare the calculated conductivity at the midpoint between three vortices with the measured bulk ZBC. This shows a very good agreement, especially taking into account that there are no free parameters in the calculation: $\xi_\pi$ is determined from the vortex profile, and $\sigma_0'$ from the zero field measurement. The vortex core overlap also explains the, strongly nonlinear field dependence of the electronic specific heat, $\gamma$ [1, 11]. In strongly type-II superconductors core overlap is usually negligible, with each vortex creating the same number of quasiparticles at the Fermi surface, and hence contributing by the same amount to the specific heat. In that case $\gamma = \gamma_n H/H_{c2}$, where $\gamma_n$ is the electronic specific heat in the normal state. However, in the case of MgB$_2$, with strong core overlap in the $\pi$-band, the isolated vortex assumption is violated. Instead, one can calculate the contribution from the $\pi$-band, simply by averaging the normalized ZBC in one vortex lattice unit cell, $\gamma_\pi = \gamma_\pi^0 (\sigma'(r, 0))$ [13]. On the other hand, the $\sigma$-band can be described by the usual linear field dependence $\gamma_\sigma = \gamma_\sigma^0 H/H_{c2}$. Adding the terms gives $\gamma = \gamma_\pi + \gamma_\sigma$, where $\gamma_\pi^0/\gamma_\sigma^0$ is the relative weight of the two bands. The calculated field dependence of $\gamma$ is shown in Fig. 3b, in perfect agreement with the measured specific heat for polycrystalline MgB$_2$ [1], using $\gamma_\pi^0/\gamma_\sigma^0 = 0.55/0.45$.

In summary, we have presented STS data on the $\pi$-band in MgB$_2$, including the first vortex imaging in this material. We have demonstrated the absence of localized states in the vortex core, a very large vortex core size and a strong core overlap. The data presents a striking experimental demonstration of the fundamentally different microscopic properties of the two bands in MgB$_2$.

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