Signature of curved QFT effects on the optical properties of deformed graphene

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Abstract – The Dirac equation in curved space is used to study the optical transmittance of deformed graphene along a given direction. Our theoretical analysis of the available experimental data for the light transmittance suggests that the periodic ripple associated with the out-of-plane deformation observed in unstrained graphene explains the observations. Furthermore, the experimental uniaxial strained graphene for light transmittance shows two features, namely the modification of the \( \cos^2 \theta \) law and the decrease of the amplitude of the oscillations with the polarization angle \( \theta \), which can be well accommodated within the theoretical analysis used here and provide further evidence of the validity of using QFT in curved space to understand two-dimensional materials.

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Introduction and motivation. – Graphene is a two-dimensional material which has been fabricated for the first time about ten years ago [1,2]. Its electronic and optical properties are typically described assuming that the electrons live on a 2D flat surface and using tight-binding models or, equivalently, the Dirac equation [3–9]. However, the experimental evidence that the graphene sheet is not a planar surface is known since the early times of graphene production [10–14]. Furthermore, \textit{ab initio} calculations [15] show that thermal fluctuations induce sizeable ripples in the graphene sheet.

From the point of view of the Dirac equation, deviations of a graphene sheet from a planar surface can be considered, at least partially, via the formulation of Quantum Field Theory (QFT) on curved spaces; see, e.g., [4,16–20] and references therein. For very large geometric deformations, the overlap between the various orbitals is changed significantly. New types of terms should be added to the Dirac Hamiltonian in order to take into account this effect in the material electronic structure [21]. For small deformations, the usual free massless Dirac Hamiltonian is the lowest-order approximation to the Dirac equation in a curved space and, hopefully, its geometric deformation can be handled by the introduction of curvature in the usual way and without appealing to new terms in the Hamiltonian.

Herein, we will investigate the optical properties of deformed (non-flat) graphene using the Dirac equation in curved space. As discussed previously, one expects that such an approach is able to describe small deformations of the graphene sheet. This is not the only possible approach and, indeed, the effect of deforming or straining has also been investigated within the tight-binding model [3,18,21]. One can start from the tight-binding model with curvature and derive a continuum Hamiltonian taking into account the deformations of the material [21–25].

In the approach based on the Dirac equation in a geometrically deformed space, the effect of curvature can be rewritten in terms of pseudo gauge fields, whose physical origin can be traced back to strain (in-plane deformations) and/or curvature (out-of-plane deformations) of the pristine material, see, e.g., [19]. These pseudo gauge fields can induce a zero-field quantum Hall effect [16], which was observed experimentally [17,26]. According to the authors, the observed pseudo magnetic fields can be as large as 300–600 tesla.

The geometric deformations of the graphene sheet, being it associated with strain or curvature, change the electronic and optical properties of the pristine material; see, e.g., [19,27–38] for theoretical predictions and [10–14,39–48] for experimental work. From the experimental point of view, the realisation of such systems
require the control of both the induced strain and the curvature of the graphene sheet. Strain and curvature appear as another tool to engineer the electronic and optical properties of graphene. Further, the considerations discussed here with graphene also apply to any material whose theoretical understanding relies on the same principles as, for example, monolayers of transition metal dichalcogenides [49].

In the present work, we will study the optical transmittance of deformed graphene from the point of view of a Dirac equation in curved space and for a (small) deformation along a single direction based on our previous publication [19]. The present study was motivated by the recent experimental work of ref. [45], which measured the optical conductivity in strained graphene using a laser with a frequency of 632.8 nm. Such a wavelength corresponds to the red light, i.e., in the visible region. For our theoretical analysis, the experimental results correspond to the infinite frequency limit of the formula derived in [19]. In the infinite frequency limit, it turns out that the optical conductivity is saturated by the interband electronic transitions. The information about the geometric deformation of the graphene sheet is resumed in the arc length (ξ) of the graphene sheet along the direction of the deformation and in a function (F) which “measures” the possible electronic transitions from the valence to the conduction band. For completeness, we will reproduce the main results of [19] such that the reader can follow the discussion and have a better insight into our results and comparison to the data [45].

This work is organized as follows. First we review the computation of the optical conductivity for deformed graphene. The special case of the small deformation is investigated in detail and general expressions, valid for any type of deformation, are derived. Furthermore, we discuss the outcome for the optical conductivity, in the limit of small deformations, for three different geometrical profiles which are used to interpret the experimental results [45]. Finally we compute the optical transmittance and discuss the available experimental results.

The theoretical framework and the optical conductivity. – In the following we will assume that the graphene layer lies on the xOy plane, i.e., its surface is defined by the equation z = 0. If the graphene sheet is deformed in some way, its surface is given by z = h(x, y). Instead of studying a general two-dimensional deformation, which includes strain and curvature, we will consider a periodic deformation along a single direction given by z = h(x) = h(x + 2π/ξ). Further, we will assume that the electronic wave functions satisfy periodic boundary conditions. Recall that for sufficiently large samples, the boundary conditions have no influence on the electron physical properties. The spatial periodicity can be seen either as having a regular structure in the deformation, which repeats every time as the position is increased by 2π/ω, with ω playing the role of “spatial angular frequency”, or as taking this distance as the full length of the graphene sample. Such type of deformations was experimentally realised in [44,45] and, in particular, in [45] the optical transmittance was measured for various deformations of the graphene.

We have shown elsewhere [19] that, by using the Dirac equation with a periodic deformation along the x-axis and within the linear response theory, the real part of the graphene optical conductivity for the interband electronic transitions in the short-wavelength limit, where the frequency of the incident light tends to infinity (Ω → ∞), is given by

$$\frac{\Re \sigma_{xx}}{\sigma_0} \rightarrow \left( \frac{2\pi}{\xi} \right)^2 + \frac{2}{\xi^2} \sum_{n=1}^{\infty} |F(n)|^2$$

for the x-direction. The universal conductivity is σ0 = e2/h,

$$F(n) = \int_0^{2\pi} du e^{i\phi(n,u)}$$

and

$$\phi(n,u) = \frac{2\pi n}{\xi} \int_0^u dv \sqrt{1 + h_x^2(v)}.$$  

The function F(n) summarizes the information on the allowed electronic transitions, together with the geometry of the graphene sheet. Note that the dependence of the conductivity on the graphene geometry comes via h_x and not the profile function h(x), i.e., the optical conductivity is sensitive to how the profile changes rather than to the profile itself. Moreover, it is the arc length ξ = ∫_0^{2\pi} dv \sqrt{1 + h_x^2(v)}, which sets the scale for the optical conductivity.

The optical conductivity associated with interband transitions reaches a plateau as the light frequency Ω increases. For planar unstrained graphene, this plateau is associated with the universal conductivity [5], so the role of the periodic curvature is to change this universal behavior along the deformed direction. Indeed, in the limit of large incident frequencies, the effects due to temperature, chemical potential and the periodic boundary condition are washed out. In the direction perpendicular to the deformation profile, called y-direction, for sufficient large Ω one has \Re \sigma_{yy}/\sigma_0 → 1. The high-frequency limit for \Re \sigma_{xx} has a plateau whose value encodes the geometry of the graphene layer.

Expansion for small-deformation limit. – Let us discuss the small-deformation limit of eq. (1) in more detail. By small-deformation limit, one considers the case in which the arc length in units of 1/ω is essential unitary. If one assumes that |h_x^2| ≪ 1, then one can approximate

$$\xi = 2\pi + \frac{\langle h_x^2 \rangle}{2} - \frac{\langle h_x^4 \rangle}{8} + \cdots$$

with \langle h_x^n \rangle = \int_0^{2\pi} dv |h_x(v)|^n.
The function $F(n)$ can also be expanded in powers of $h^2$ and, after some straightforward algebra, the optical conductivity becomes

$$\frac{\Re \sigma^{\text{inter}}_{xx}}{\sigma_0} = 1 + \delta_{xx},$$

(5)

where

$$\delta_{xx} = -\frac{\langle h_x^2 \rangle}{2\pi} + \frac{1}{16\pi^2} \left[ 3\langle h_x^2 \rangle^2 + 2\pi\langle h_x^4 \rangle \right]$$

(6)

It follows from eq. (6) that for small deformations of the graphene sheet, the optical conductivity is reduced relatively to the planar material value and the optical transmittance is increased. Graphene becomes more transparent for large frequencies with deformation.

In order to try to understand how deformations change the optical conductivity, let us consider the following profiles:

$$h_1(x) = A \sin(\omega x),$$

(7)

$$h_2(x) = A \exp \left\{ -\frac{(\omega x - \pi)^2}{2\sigma^2} \right\},$$

(8)

$$h_3(x) = A_1 \omega_1 x (\omega_1 x - 2\pi) + A_2 \sin(\omega_2 x),$$

(9)

amely ripple ($h_1$), Gaussian ($h_2$) with width $\sigma$ and deformation ($h_3$). The experimental results of [45] will be analysed using these three different profiles.

The optical conductivity, as given by expression (6), for the profiles $h_1, h_2$ (with $\eta = A \omega$) and $h_3$ (with $\eta = A_1 \omega_1$ and $A_2 = 0$) can be seen in fig. 1. As concerns the comparison between the ripple and the Gaussian bump, as shown in the upper frame of the figure, it turns out that the ripple has typically the smallest conductivity (highest transmittance). On the other hand, the deformation associated with $h_3$ seems to be associated with an even smaller value of the conductivity when compared to the ripple profile, as seen in the middle frame. The rapid increase in the conductivity observed in fig. 1 for the $h_2$ and $h_3$ profiles is related to the validity of the approximation used in the calculation. For illustration we show in the bottom frame, the comparison between the ripple and Gaussian profiles.

**Optical transmittance.** – The transmittance is defined as the ratio between the outgoing and incoming light intensity and it is given by $T = |T_{xx}| \cos^2 \theta + |T_{y y}| \sin^2 \theta$, where $\theta$ is the polarization angle, i.e., the angle between the electric-field component of light and the direction associated with the deformation $x$, and

$$|T_x| = \frac{1}{\left(1 + \pi \alpha \frac{\Re \sigma^{\text{inter}}_{xx}}{\sigma_0}\right)^2} \approx 1 - \pi \alpha \frac{\Re \sigma^{\text{inter}}_{xx}}{\sigma_0},$$

(10)

to first order in the fine-structure constant $\alpha$. For small deformations one can write

$$\frac{\Re \sigma^{\text{inter}}_{xx}}{\sigma_0} = 1 + \delta_{xx},$$

(11)

and the transmittance becomes

$$T = T_0 - \pi \alpha \delta_{xx} \cos^2 \theta,$$

(12)

where $T_0 = 1 - \pi \alpha \approx 97.7\%$ is the transmittance of pristine graphene [50]. To first order in the deformation it follows that

$$\delta_{xx} = -\frac{\langle h_x^2 \rangle}{2\pi},$$

(13)

and the geometric deformation increases $T$ relatively to the planar graphene.

**Unstrained graphene.** The optical transmittance for graphene and for deformed graphene was measured, as a function of the polarization angle $\theta$, in [45]. For plane graphene, the experimental values for $T$ at various locations of the graphene sheet can be seen in fig. 2. The experimental data for $T$ is consistent with the functional form (12). For each data set in fig. 2, a fit to $\alpha + b \cos^2 \theta$ gives the parameters presented in table 1, where the

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parameters are labelled by the color of the corresponding data set used in the fit.

In our analysis the quoted errors on the coefficients $a$ and $b$ are associated purely to the fit. The values of the $\chi^2$/d.o.f. are quite small but seem to support that $T$ is well described by eq. (12). We call the reader attention to the fact that the value for $a \approx 0.976$ is quite close to the theoretical estimate $T_0 = 0.977$.

From fig. 1 of ref. [45] a very crude estimate of the parameter $b$ can be made. Indeed, reading from the figure and assuming a ripple shape, it follows that $A_{\exp} \sim 90$ nm and $2\pi/\omega_{\exp} \sim 2.5 \mu$m giving $\eta_{\exp} = A_{\exp}\omega_{\exp} \sim 0.2$. The results of the fits using the ripple profile (7) give $\eta = 0.28$ (black), 0.24 (red), 0.29 (magenta) and 0.30 (blue), which are in the same ballpark as the very crude estimate obtained directly from the figure of the graphene slab [45].

In the analysis we assumed that the deformation of graphene is a ripple structure and, therefore, we only considered so far the profile $h_1$. However, the experimental data is also compatible with the profiles $h_2$ and $h_3$.

In fig. 3, we show the allowed range of parameters for the various profiles compatible with the interval of values coming out from the fits to the experimental transmittance reported in fig. 2. As we have already discussed, the ripple profile $h_1$ suggests a value for $\eta$ that is compatible with the crude estimate from the actual graphene sample giving $\eta_{\exp} \sim 0.2$ (see upper frame in fig. 2).

The allowed range of fitting parameters of the Gaussian profile $h_2$ is shown in the middle frame of fig. 2 and it seems to favour $\eta \geq 0.5$, if one assumes small deformations of graphene. Such value for $\eta$ is hardly consistent with $\eta_{\exp}$. On the other hand, the quadratic profile $h_3$ with $A_2 = 0$ has a parametric region consistent with $\eta_{\exp}$, as shown in the bottom frame of the figure.

From the analysis of the various profiles and relying on the comparison between the allowed values of $\eta$ and $\eta_{\exp}$, see table 1, one concludes that experimental data favours the ripple and the quadratic structures.

**Uniaxial strained graphene.** In ref. [45] the graphene optical transmittance was measured both for unstrained and strained material. The data for this latter case were obtained by bending the graphene layer and can be seen in fig. 4. The isotropy of the hexagonal lattice elasticity
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Fig. 4: (Color online) Transmittance for a bended graphene layer. Experimental data from fig. 3-b of ref. [45], where $\varepsilon$ is the strain fraction along the bending direction. The dotted lines guide the eyes through the experimental data with $\varepsilon = 0.5\%$ and $0.7\%$. The solid curves are our fittings to the data with $\varepsilon = 0$ (black line: large amplitude) and $\varepsilon = 0.3\%$ (red line: small amplitude).

allows to define the strain tensor to lowest order in terms of the uniaxial strain $\varepsilon$, the associated bending direction with respect to the zig-zag direction, and the Poisson ratio. The experiments reported in ref. [45] were performed for $\varepsilon = 0.3\%$, $0.5\%$ and $0.7\%$. The model based on quantum field theory in curved space is valid for small deformations and we focus on flat graphene and on the deformation for $\varepsilon = 0.3\%$.

We would like to mention that the effects of in-plane deformations associated to strain and out-of-the plane deformations on the optical conductivity of graphene-like materials, within the formalism of a Dirac equation in curved space, were explored in ref. [51]. In our analysis of the experimental results, the contributions of in-plane deformations and of possible changes in the Fermi velocity of the electrons are not taken into account.

The data characterized by $\varepsilon = 0.3\%$ follows the same pattern as observed for unstrained graphene, with the transmittance being compatible with a $\cos^2 \theta$-dependence with the polarization angle. The data shows a decrease on the oscillation amplitude with respect to the unstrained case, and the fitted value of $b$ is somewhat smaller than the ones presented in table 1. Indeed, the fit to the data gives $a = 0.975909(30)$, $b = 0.000576(47)$ for a $\chi^2$/d.o.f. $= 6 \times 10^{-9}$. In terms of $b$, the deformation implies a reduction of its value by about 50% when compared to the unstrained case. This can be accommodated within the profile $h_3$, which combines the ripple structure considered previously with a smooth quadratic type of deformation, if one takes $\eta_2 = A_2 \omega_2$ slightly smaller than the corresponding outcome for the red points in unstrained graphene ($\eta = 0.24$) and assumes that the quadratic part of the profile $h_3$ simulates the bending of the graphene layer. Figure 5 shows the allowed parameter range compatible with $b = 0.0005$ and a 10% relative error; in the figure $\gamma = \omega_1/\omega_2$. The data clearly favours small values of $\eta_1 = A_1 \omega_1$ ($<0.02$), but leave $\omega_1$ essentially unbounded.

This allows us to identify $\omega_1$ with the curvature induced by the bending of the graphene layer.

The range of estimated parameters ($\eta$, $\gamma$, $\omega_1$) allowed from the analysis of the data for the strained graphene can be accommodated within our theoretical description of a strained graphene layer. Further, the estimated values are also compatible with those provided from the analysis of the unstrained case.

Conclusions. — The consistency between the quantitative and qualitative analysis of the light transmittance observed for unstrained graphene and the quantum field theory framework in curved space suggests that the light transmittance is determined by the ripple structure of the graphene sheet. For strained graphene and small enough deformations, the experimental data is well reproduced by a geometrical deformation of the graphene sheet which takes into account the ripple structure, as observed in the unstrained case, together with a smooth deformation of the original material, parametrized in our case by a quadratic function which adds to the sinusoidal ripples.

The analysis performed here shows once more that the field-theoretical framework in curved spaces can be a useful tool in the investigation of electronic and optical properties of graphene or, from another point of view, it offers the possibility of engineering graphene to study quantum mechanics in deformed space-times at tabletop experiments.

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