Student networks on online teaching due to COVID-19: Academic effects of strong friendship ties and perceived academic prestige in physics and mathematics courses

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Collaboration among students is fundamental for knowledge building and competency development. Nonetheless, the effectiveness of student collaboration depends on the extent that these interactions take place under conditions that favor commitment, trust, and decision-making among those who interact. The sanitary situation and the transition to remote teaching has added new challenges for collaboration given that students’ interactions are mediated by Information and Communication Technologies (ICTs). In this study we explore the effectiveness of different collaborative relationships on physics and mathematics, from a sample of secondary students from two schools located in rural and urban areas in southern Chile. We used Social Network Analysis (SNA) to map students’ friendships relations, academic prestige, and collaboration on both courses. Later we combined the collaboration network with friendship and academic prestige on the course, to separate strong from weak friendship working ties, and those among students who enjoy or not academic prestige. Multiple linear regression models showed, on average, positive effects of collaboration on grades. Yet, when isolating the effects of the types of collaboration, the positive effects are observed only between those who display more strong friendship ties. Also, we found differences on the social networks and their effects over grades between both courses, presumably due to their pedagogical nature. With these results we contribute to the literature of collaboration and its effectiveness based on the nature of students’ relationships, and advocate for the importance of instructional design in fostering appropriate motivations and guidelines for constructive collaboration in the classroom.

I. INTRODUCTION

Student collaboration is increasingly gaining attention for its benefits on learning and overall human development [1-3]. Education scholars and policy makers have highlighted teamwork and social competencies as key abilities for life and work in the XXI Century [4, 5]. The emphasis on social skills is necessary to equip individuals with creative capacities in the face of complex and multidisciplinary challenges [6]. The worldwide pandemic due to COVID-19, has without a doubt added external difficulties to the development of collaborative skills, as schools and universities were forced to move from face-to-face to remote instruction, and with the subsequent changes in students’ roles and means for socialization and interaction.

Remote teaching implies that students’ communication is mediated via Information Communication Technologies (ICTs) [7,9], such as forums, chats, emails, or video conferences among other alternatives. Even though technologies are ubiquitous in today’s society, the effectiveness of remote education strongly depends on their accessibility to technology, and on their readiness to navigate and deal with these with autonomy and self-regulation [10, 11]. These conditions clearly affect how students’ engage in forums or chats, instances that become proxies of social engagement and collaboration [8, 12, 13]. Yet, engaging on effective collaboration implies finding the right partners to work with, which depends on assessing a myriad of variables related to the nature of the learning activity and its requirements [14], and the trust and commitment embedded in one’s working relationships (i.e., friendship) [15]. Here, the use of Social Network Analysis (SNA) affords relevant methodological and theoretical tools to capture the different types of social relationships they engaged on in the classroom, and how these foster (or hinder) their learning potential [16].

Consequently, and with the goal of further understand effective collaboration in physics and mathematics in remote classrooms, we turned to SNA [17, 18] to explore the academic effects of having working social ties with friends and/or other prestigious students. Based on students’ social network we characterize different collaborative relationships depending on whether these occurred among friends (i.e., strong), in the absence of friendship (i.e., weak), and
between proficient peers. This work contributes first, with a novel method to categorize students’ working relationships following SNA, and second, with empirical evidence that shows the academic gains of various collaborative ties under distinctive teaching methodologies enacted in physics and mathematics (i.e., lecture-based and active learning).

II. STUDENT NETWORKS AND TEACHING STRATEGIES

Using SNA on education has enabled researchers to understand the benefits of student collaboration from the logic of social capital, in the sense that a greater number of social interactions -high network centrality- allows access various forms of resources and information, and the potential adoption of behaviours related to success [19][20]. Good performance has been found linked to students’ social networks on face-to-face [20][23] and remote course [8][24][25], while covering a wide range of topics and strategies. Such findings align with the sociocultural view of cognitive and human development, as knowledge is constructed while learners work alongside others who could potentially expand the frontiers of their individual achievements, on what has been defined as the Zone of Proximal Development (ZDP) [26].

The benefits of having multiple interactions with peers on the classroom, and becoming a central member of the network extends to other variables related to achievement, such as retention [27][29], and self-efficacy, or the believe on one’s abilities to successfully meet the academic and performance expectations [30]. Besides, programs grounded on the principles of collaborative learning have shown important results for developing social skills [31], and trust among team members, which increases the likelihood of group effectiveness [32].

Nonetheless, more recent evidence on SNA on university physics courses suggests that the academic gains from having multiple working ties depend on the nature of the learning task [22]. Accordingly, a great number of social ties relate to having a worse performance on well-defined physics problems (e.g., textbook problems), whereas open-ended and creative activities benefit from multiple social ties connecting different groups (i.e., brokering knowledge [22][33]). Additional results on primary education found that having multiple ties is again linked with poor performance, while the reciprocity of students’ relationships becomes the necessary condition for higher achievement [34].

Furthermore, according to evidence on sociology and networks, the nature of the social relationship plays a key role in acquiring and developing knowledge depending on its complexity [35][36]. For instance, new tacit, factual or knows what type of information is easily accessible through weak social ties, that is, among individuals who do not share a sense of commitment nor are deeply embedded into the relationship [35]. The key consideration is that weak ties are observed between individuals who do not belong to one’s cohesive groups -governed by strong relationships-, and are therefore preferable for accessing simple new ideas outside such groups. On the contrary, strong ties are better suited for learning complex and non-tacit ideas, because developing such knowledge requires a social commitment and a common language to transfer the intricacies of this new information [36]. Such learning considerations are frequently observed among individuals who share a strong relationship, like friends.

All of the above stresses out the challenges of guiding students’ collaboration in the classroom, taking into account the nature of the tasks and information to be learned. These complexities are now relevant in this transition to remote teaching, where students’ interactions are mediated by ICTs [8]. Studies on remote learning have conceptualized students’ course participation using traditional methods, such as the number of posts on online forums [7][12], the time dedicated to reading comments [13][37], or via content analysis of the posts written [38]. Recently, researchers have used SNA to explore different forms of participation on online courses. For instance, Traxler, Gavrin and Linden [8] conceptualized students’ co-occurrence of posts on discussion forums, which were defined as the links on the participation network, and later used to determine and understand students’ centrality based on their access to the ideas presented. Under this condition, higher access to information on forums, that is, high network centrality is positively correlated with academic success [8]. Through similar network methods, an additional study has found positive correlations between students’ participation on online courses -centrality- with their sense of belonging [25]. Yet, the centrality on this participation network offers positive effects specially to high performance students, as content analysis has shown that their discussions circled around conceptual aspects of the course content, whereas the discussion networks formed by low performing students tend to focus on practical and superficial elements of curriculum [39].

From the perspective of learning methodologies, active classrooms have shown higher levels of social interactions compared to traditional lecture-based instruction [22][40][43]. Student-centered classrooms favor autonomy over the learning process through peer interaction, because these tend to include activities designed to encourage decision-making, content manipulation and communication, thus allowing students to perceive learning as a construction mediated by collaboration [14][22]. The social and cognitive attributes of activities implemented on active learning methodologies are also recommended on virtual classrooms [44][47], because these encourage higher levels of academic achievement and digital competencies [48].

Finally, the work of Johnson, Johnson and Holubec [49] on student collaboration adds fundamental conditions for group effectiveness: positive interdependence, or the belief that the success is a collective rather than individual effort; and personal responsibility for learning and engaging on one’s tasks. According to social network research on education, the above conditions are modulated by the nature of the learn-
ing tasks. For instance, close-ended well-structured physics problems hinders positive independence, as students report addressing these activities by engaging in social interactions aimed at finding the right equation or variable to use [14]. On the contrary, real-world problems [50] such as generative activities [14], motivate collaborative strategies that align with the mentioned characteristics for effectiveness. Among the reasons why one would witness such a different form of collaboration on these two sets of problems -close-ended and generative- links with their embedded attributes. Accordingly, well-structured and close-ended problems are perceived as non-additive tasks [51], given that when worked on groups these tend to be solved by the most capable team member. These problems also relate to rather simplistic cognitive processes (e.g., apply content) according to a taxonomy of physics problems developed by Teodorescu and colleagues [52]. Differently, generative activities are intrinsically additive [51], because they require collective efforts for content manipulation, decision-making and manipulation, and thus demand high-level cognitive skills [52][53].

### III. METHODS

#### A. Research Context

The study was conducted during the second semester of 2020 on a sample of secondary students from parallel classes (A & B), and from two schools in southern Chile (Sch-1 & Sch-2). This exploratory research focused on the courses of physics and mathematics. Table I summarizes the schools’ characteristics, such as the student population, research participants, location and education. Research participants gave consent via an online survey designed for this study, and where we explain the analytical procedures along with privacy considerations. A total of 101 students agreed to be involved in the study, with 45% of female participants.

During 2020 and due to the COVID-19 pandemic, both schools adapted their teaching methodologies by introducing different ICTs. Initially, on School 1 teachers began the academic year with asynchronous sessions using content videos shared via text messaging apps (e.g., WhatsApp). After two months, School 1 implemented synchronous 40 min sessions organized on MEET and CLASSROOM learning management systems (LMS). This scenario differed from School 2, where remote teaching began with 1-2 hours synchronous course sessions a week after the school canceled face-to-face instruction. These sessions, similar to School 1 were organized on the same LMS.

In addition to the initial organizational differences, both schools organized and taught physics and mathematics content following opposite learning methodologies. In School 1, lecture-based instruction was the main methodology on both courses, followed by problem solving sessions where students faced well-structured activities (e.g., textbook problems), and were later assessed on their individual work. In School 2, the mathematics course met the characteristics of School 1 with 3 weekly classes, but with the difference that sessions were 1-2 hours long compared to 40 min on School 1. Finally, physics on School 2 was based on active learning methodologies, including generative activities [14], where students, for instance, working on groups designed videos centered around physics concepts and phenomena. The physics classes met once a week for 40 min and 1 hour respectively for Schools 1 and 2.

#### B. Data Collection

Because the study aims to determine the academic effects of different collaborative relationships on school physics and mathematics, we collected final grades from the year prior to the study (2019), along with students’ grades on the second semester of 2020. In 2020, students’ performance on both courses on School 1 accounted for in-class activities (e.g., problem solving) and individual testing. This is similar to how mathematics’ grades were obtained in School 2. Lastly, physics grades on School 2 consisted on the assessment of the generative activities (e.g., content videos and physics posters), which consisted on grading their structure and organization, language and theory, including a peer evaluation of the groups’ performance.

Finally, student collaboration was measured through online network surveys, shown to be a reliable mechanism for network mapping [17]. This survey was designed to gather different social relationships: friendship ties; prestige on physics and mathematics; and collaboration on physics and mathematics. The survey was constructed using the class’ roster, which has been utilized in previous studies to facilitate responses for network measuring [16][22][40].

#### C. Data Analysis

From the network survey we identified key variables to characterize the groups in terms of their friendship relations, prestige and collaboration on both physics and mathematics courses. The survey yields an indirect network, that is, where ties are not necessarily reciprocal (e.g., A selects B as a friend, but B does not select A as a friend). Tables II summarize the mean of key descriptive network variables for each of the social dimensions measured on the survey. The variables include the number of students per group, or nodes, the total number of ties observed, the average number of ties

| Sch1 | Students | Participants | Location | Education |
|------|----------|--------------|----------|-----------|
| Sch2 | 906      | 46           | Urban    | Scientific & Humanistic |

Table I. School attributes and characteristics
or average degree, and network density –percentage of ob-
erved ties considering 100% as if all nodes on the network 
were connected to each other [17, 18].

We operationalized collaboration as degree centrality on 
the collaboration network, or as the total number of ties. De-
gree centrality accounts for both incoming and outgoing ties, 
named indegree and outdegree centrality respectively. The 
former indicates the number of ties headed from nodes on the 
network towards a focal actor, whereas the latter accounts for 
relationships declared by the focal actor towards other nodes 
on the network. Besides this definition of the variable Col-

laboration (see Table [III], we combined friendship, prestige 
and collaboration networks to identify different types of col-
laborative relationships among students. We turned to the 
strength of ties terminology used on the social network lit-

erature to differentiate between strong and weak collabora-
tives like grades on the year prior to the study, School, and 
effect of collaboration over grades, we include control vari-
ables constructed and used for the analysis.

It is worth mentioning that each of the five variables shown 
on Table [III] were built for their respective course (i.e., physics 
or mathematics). For instance, the collaboration network on 
mathematics, along with academic prestige on the same 
course and friendship were combined to determine the five 
collaborative ties described above for mathematics, and the 
same occurs for physics with its respective networks. Later, 
we used ordinary least squares multiple regressions models 
(OLS) to predict grades on both courses, while using collab-
oration variables as the main predictors. In order to isolate the 
effect of collaboration over grades, we include control vari-
ables like grades on the year prior to the study, School, and 
gender (female). Finally, as a robust check, we fitted hier-
archical linear models to account for the class and schools’ 
variance. Results here did not differ from the multiple regres-
sion models.

IV. RESULTS

A. Collaboration and Grades on Physics

Figure 2 depicts the collaboration networks of all four 
classes from Schools 1 and 2. The networks show four types 
of ties based on whether students display strong or weak re-

lations with others, who at the same time might or not enjoy 
academic prestige in physics. Beside, the network depiction 
illustrates grades in shades of green, as well as degree cen-
trality as the nodes’ size.

A first look of these networks allows a visual representa-
tion of the information contained on Table [III] where classes 
Sch1-A and B have low network density, represented by the 
reduced number of ties compared to School 2. Plus, there 
are differences between groups in School 1, as in class A 
we observe an abundance of social relations of diverse na-
ture spanning most of the students, whereas class B seems to 
be governed by strong ties with prestige (blue links) and with 
many isolated members. In this last group, connected stu-
dents with high centrality appeared with the highest grades, 
differently from Sch1-A, where good grades are not an ex-
clusive attribute of central individuals. Finally, both networks 
on School 2 show an even distribution of good grades, while 
their ties are mainly strong.

The multiple regression models fitted to predict physics 
grades are shown on Figure 3. On model A we used degree 
centrality of the collaboration network as the main predictor, 
yielding a positive coefficient (.29, p < .01) and thus, sug-
gesting that more working partners foster success in physics. 
When differentiating the effects of types of collaboration, 
model B shows a null effect for weak ties, while having 
strong relationships indicates a positive predictive value over 
physics performance (.27, p < .05). When adding academic 
prestige, models C and D show no significant gains of work-
ing alongside others who are perceived as good physics stu-
dents. Finally, it is worth highlighting the predictive value of 
prior grades on physics across all four models, and the mean 
difference between Schools’ 2 and 1 in favor of the former.

B. Collaboration and Grades on Mathematics

Similar to what was shown in physics, the mathemat-
ics networks on Figure 4 depicted the different levels of so-
cial connectivity between groups and schools. However, 
across groups, nodes with higher degree centrality enjoy bet-
ter grades. Additionally, in both classes from School 1 there 
are an important number of weak ties between students not 
recognized as prestigious, plus a similar number of isolated 
nodes. Importantly, good grades are observed among those 
who display strong collaborative ties, with either other good 
students or not. Differently, in School 2 it is possible to dis-
tinguish mainly strong social ties among students who get a 
higher grade, whereas low performance seems linked to weak 
interactions.

Figure 5 shows the multiple regression models for mathe-

matics grades. Similar to physics, there is evidence on model 
A that having more collaborative partners (degree) relates to 
better outcomes on math (.38, p < .01). Yet, these aca-
demic gains are observed among those who interact with their 
friends (strong ties, .36, p < .01) rather than among stu-
dents who work away from the close social circles (weak
Table II. Descriptive statistics of directed networks: Friendship, Physics Prestige, Collaboration on Physics, Mathematics Prestige, and Collaboration on Mathematics.

| Group | Nodes | Ties | Degree* | Density | Ties | Degree* | Density | Ties | Degree* | Density | Ties | Degree* | Density |
|-------|-------|------|---------|---------|------|---------|---------|------|---------|---------|------|---------|---------|
| Sch1-A | 29    | 132  | 4.55    | 0.16    | 54   | 1.86    | 0.07    | 43   | 1.48    | 0.05    | 84   | 2.9     | 0.1    |
| Sch1-B | 26    | 95   | 3.65    | 0.15    | 67   | 2.58    | 0.1     | 49   | 1.89    | 0.08    | 88   | 3.39    | 0.14   |
| Sch2-A | 23    | 194  | 8.44    | 0.38    | 126  | 5.48    | 0.25    | 52   | 2.26    | 0.1     | 138  | 6       | 0.27   |
| Sch2-B | 23    | 151  | 6.57    | 0.3     | 128  | 5.67    | 0.25    | 55   | 2.39    | 0.1     | 157  | 6.38    | 0.31   |

* Average degree, or average number of incoming plus outgoing ties per student on the class.

Figure 1. Diagram shows the methodology utilized to identified and construct collaborative variables number 2, 3, 4 and 5 described in Table III.

Table III. Types of collaborative relationships and definition

| Type of Collaboration | Definition |
|-----------------------|------------|
| 1. Collaboration      | Degree centrality of the collaboration network, or number of collaborative ties. |
| 2. Strong             | Number of collaborative ties between students who are friends. Friendship is observed on the network when at least one of the actors on the dyad indicates the other as a friend (e.g., A → B). |
| 3. Weak               | Number of collaborative ties between students who do not declare themselves as friends. |
| 4. Strong w/ Academic Prestige | Number of collaborative ties between friends and who are perceived by the other as a good student on the course. Friendship is observed on the network when at least one of the actors on the dyad indicates the other as a friend (e.g., A → B). Similarly, prestige comes from its respective network and when at least one of the actors on the dyad selects the other as a good student on the course (e.g., B → A, then B enjoys academic prestige). |
| 5. Weak w/ Academic Prestige | Number of collaborative ties between students who do not declare friendship ties among themselves, yet one of the actors on the dyad declares the other as a good student. |

Results show clear differences in the density of collaboration and friendship ties between both schools. This contrasting scenario might be attributable to the socioeconomic and cultural characteristics found on both student populations. Even though we do not count with information about students’ social or economic capital, schools’ geographical loca-
The teaching methodologies enacted by teachers in each of these classrooms might also allow us to interpret the observed differences on the number of social relationships across schools. Mathematics at both institutions and physics at School 1 were taught in a traditional fashion, with lectures and well-defined problems, similar to textbook activities students worked on individually. As found in the literature, well-defined problems introduced as group activities tend to favor isolated work and diminish collaboration due to its lack of positive interdependence [14, 51]. This pedagogical model centers around the teacher rather than their students, and encourages them a passive role grounded on individual performance [14], and might have hampered their motivation and the need to expand their existing collaboration and friendship networks for success. Therefore, such learning might help them to fortify rather than diversify students’ social networks in the classroom.

Conversely, the teaching methodology implemented on the physics course on School 2 was active and student-centered, and where participants engaged in collective creative processes for instance, to develop physics videos and posters. These educational conditions might have contributed to the density of collaborative interactions, given that the generative group activities enacted here are characterized by encouraging high levels of decision-making [52] and positive interdependence among team-members [49]. Further, research evidence has shown that active learning methodologies are preferred over lecture-based classrooms at fostering social relationships [43]. Finally, and because collaborative, friendship and prestige networks were measured months after the first generative activity was implemented, its social effects could have extended to the mathematics course, and the reason why both disciplines on School 2 display high network density.

The multiple regression models show the expected results of having multiple working peers in the classroom, which align with the benefits of social integration on education [54]. The observed learning gains are also consistent with sociocultural theory [26] and the principles of social capital [55], in the sense that social relationships enable access to information and ease collective learning, on this context, pertaining to physics and mathematics knowledge. Nonetheless, when...
examining the academic effects of different collaborative relationships, strong friendship ties showed an advantage compared to weak ties observed among those who do not declare to be friends. This evidence suggests that the physics and mathematics information and behaviors needed for a successful performance is better developed by working with closely related individuals. Consequently, the content addressed and assessed on both courses presents enough complexity that its learning requires strong friendship ties, as suggested by Hansen [36], and because individuals on cohesive networks based on trust and mutual commitment share common forms of communication and understanding to invest time and energy on their collective growth. These claims are also supported by the null effects of weak ties across all regression models, given that these social relationships are preferred for learning simple and tacit knowledge [35], a type of information that does not seem relevant in these learning contexts.

The evidence related to academic prestige requires an important consideration. According to the regression models, collaboration with friends who are perceived as good students (strong with prestige) becomes a positive predictor on mathematics, yet its effect is null on physics. Such differences might be attributable to the teaching methodologies and assessments enacted on both courses. On the physics course on School 2, students worked on groups to address collaborative activities that have shown to encourage social interactions [40-43], which could have enable students to develop friendship and perceptions of proficiency beyond their initial social networks. This teaching orientation has shown to hinder the advantages of academic hierarchies, as the collaboration networks are not governed by clusters of proficient friends. In contrast, and as mentioned earlier, the individualistic teaching methodology observed in mathematics seems to accentuate the existing networks and the advantages of already having working ties with good students, thus fortifying the social and academic hierarchies in the classroom.

Consequently, due to the creative and collaborative nature of the activities designed for physics in School 2, it is possible that participants were able to extend their own conceptions of proficiency beyond the traditions of solving well-structured problems, thus recognizing a larger number of good students in such a category. Such re-conceptualization of academic prestige enabled them to limit the gains of academic hierarchies, in the sense that proficiency is no longer exclusively associated with having good grades. This argument has been explored in the physics education literature, where prestige is
Figure 4. Collaboration network for mathematics. Node color represents academic performance, while its size is degree centrality – number of collaborative ties. Edge or link colors depict the type of collaborative relationship.

associated with activities centered around textbook-types of problems, yet not with creative and generative tasks [22].

Plus, results allow us to characterize the observed network differences in terms of variables like belonging, trust and self-efficacy and the role teaching methodologies have on fostering them. According to the evidence, active learning methodologies foster higher degree centrality than lecture-based instruction. Research studies have suggested that under the former learning conditions students achieve higher sense of belonging [25], and self-confidence to face academic tasks [28, 55]. This interpretation adds up the findings and support for the design and use of students-centered and collaborative teaching strategies, for both remote [44–47] and face-to-face classrooms [14].

Finally, the limitations of the study relate to the absence of information for instance, on internet connectivity, accessibility and teacher and student training on ICTs, given the major role these play in remote education. Besides, we recognize that the conducted study does not account for students’ personal experience during the transition from face-to-face to online instruction. Here, qualitative information and analytical tools might have provided valuable information to either support or reject the interpretations described in the paragraphs above. Furthermore, the study pretends to encourage the research and teaching community to reflect and pursue new studies and interventions on the interplay between students’ networks, teaching methods and learning. This avenue of research is promising, particularly since social and collaborative skills are nowadays necessary for human development and to face the complex challenges of the XXI Century [4, 6].

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Figure 5. Multiple linear regression models for mathematics grades. Positive coefficients are depicted in blue, and negative coefficients in red. Note: * $p < .05$ and ** $p < .01$.
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