Abstract—This paper depicts a brief revision of Generalized Regression Neural Networks (GRNN) applications in system identification and control of dynamic systems. In addition, a comparison study between the performance of back-propagation neural networks and GRNN is presented for system identification problems. The results of the comparison confirms that, GRNN has shorter training time and higher accuracy than the counter-part back-propagation neural networks.

Index Terms—Generalized Regression Neural networks; system identification; intelligent control

I. INTRODUCTION

Artificial Intelligence (AI) has a significant impact on the current research trends due its numerous applications in different aspects of the life. Artificial Neural Networks (ANNs) are one of the major parts of AI. ANNs have different applications including regression and approximation, forecasting and prediction, classification, pattern recognition and more. ANNs are useful since they can learn from the data and they have global approximation abilities. A feed-forward neural network with at least single hidden layer and sufficient number of hidden neurons can approximate any arbitrary continuous function under certain conditions [1]. ANNs have two main types: the Feed Forward ANNs (FF ANNs) in which the input will only flow to the output layer in the forward direction and the Recurrent ANNs (RANNs) in which data flow can be in any direction. Generalized Regression Neural Networks (GRNN) [2] are single-pass associative memory feed-forward type Artificial Neural Networks (ANNs) and uses normalized Gaussian kernels in the hidden layer as activation functions.

GRNN is made of input, hidden, summation, division layer and output layers as shown in Fig. 1.

When GRNN is trained, it memorizes every unique pattern. This is the reason why it is single-pass network and does not require any back-propagation algorithm.

After training GRNN with adequate training patterns, it will be able to generalize for new inputs. The output of GRNN can be calculated using (1) and (2).

\[
D_i = (X - X_i)^T (X - X_i) \tag{1}
\]

\[
\hat{Y} = \frac{\sum_{i=1}^{N} Y e^{(-D_i/2\sigma^2)}}{\sum_{i=1}^{N} e^{(-D_i/2\sigma^2)}} \tag{2}
\]

where \(D_i\) is the Euclidean distance between the input \(X\) and the training sample input \(X_i\), \(Y\) is the training sample output, \(\sigma\) is the smoothing parameter of GRNN.

GRNN advantages include its quick training approach and its accuracy. On the other hand, one of the disadvantage of GRNN is the growth of the hidden layer size. However, this issue can be solved by implementing a special algorithm which reduces the growth of the hidden layer by storing only the most relevant patterns [3].

In this paper a brief review of the applications of GRNN in modeling and identification and control is provided. A comparison also is conducted between the GRNN and back-propagation neural networks for various benchmarking problems. The rest of the paper is structured as follows: section II provides a review of the applications of GRNN in system identification and modeling, section III offers a review of the GRNN applications in control systems, section IV contains the results of GRNN and back-propagation neural networks comparisons and their discussions and finally section V contains conclusions of the research.
II. APPLICATIONS OF GRNN IN MODELING AND SYSTEM IDENTIFICATION

GRNN can be used as identifier for a given plant dynamics or a process. To use GRNN as identifier it should be given the plant/process inputs and outputs and then it will predict the plant/process output. GRNN identifier is shown in Fig. 2 where $Y$ represent the actual plant output and $\hat{Y}$ is the predicted plant output.

Since GRNN is a regression-based neural network, it is widely used for approximation, fitting, prediction and regression problems including process modeling and monitoring [4], modeling of dynamic plants [5], aerodynamic forces prediction [6], prediction of voltage variations in power plants [7], prediction of performance and exhaust emissions in internal combustion engine [8], solar photo voltaic power forecasts [9], traffic accidents prediction [10], nonlinear radio frequency systems modeling [11], predictive modeling of nonlinear systems [12], modeling of microwave transistors [13] and identification of a quadcopter dynamics [14].

III. APPLICATIONS OF GRNN IN CONTROL SYSTEMS

In addition to its application in system identification and modeling, GRNN can be used as intelligent adaptive controller. GRNN can be used in control systems either off-line or on-line. If it is used off-line, it needs to be trained to work as inverse dynamics and then it will be deployed into the on-line system. The second approach is using GRNN controller on-line from the beginning so it will adapt to the error signals on-line. In the second case an adaptation algorithm is required to adjust GRNN parameters. The second approach is shown in Fig. 3.

Some of the applications of GRNN in control systems include dead-zone estimation and compensation in motion control of a traveling wave ultrasonic motor [15], fault diagnosis of power system [16], intelligent battery charger [17], microgrid hybrid power systems control [18], bipedal standing stabilization [19], air conditioning control [20], wind generation system [21], helicopter motion control [22], active vibration control [23], active noise cancellation [24], rat-like robot control [25], pipe climbing robot control [26], tracking-control for an optomechatronical Image derotator [27], tracking in marine navigational radars [28], factory monitoring [29], and flapping wing micro aerial vehicle control [30].

IV. GRNN VS BACK-PROPAGATION ANN

In this section a comparative study is conducted between the GRNN performance and a Back-Propagation (BP) FFANNs in the training stage.

The deployed datasets are provided by Matlab Mathworks [30] as a benchmarking data for ANNs performance measuring. Here are descriptions of the used datasets:

- The simple fit dataset is a 1-input/1-output fitting dataset and it contains 94 observations.
- Abalone shell rings dataset is 8-input/1-output fitting dataset and it contains 4177 observations. The ANN should estimate the number of shell rings in abalone based on the 8-inputs.
- Building energy dataset is 14-input/3-output fitting dataset and it contains 4208 observations. The ANN should approximate the energy use in a building based on the given 4-inputs.
- Cholesterol dataset is 21-input/264-output fitting dataset and it contains 4208 observations. The ANN should estimate the Cholesterol levels in the body based on the 21-inputs.
- Engine dataset is 2-input/2-output fitting dataset and it contains 1199 observations. The ANN should estimate the engines torque and emissions based on the given 2-inputs.
- Cancer dataset is 4-input/3-output classification dataset and it contains 150 observations. The ANN should classify the type of cancer based on the 4-inputs.
- Thyroid dataset is 21-input/3-output clustering dataset and it contains 7200 observations. The ANN should classify the patient as normal, hyperfunction or subnormal functioning based on the given 21-inputs.

The Mean Square Error (MSE) and the training time are recorded for both of BP ANN and GRNN for different datasets and shown in Table I.

MSE is a prominent performance measure in ANNs. It can be calculated using the following equation:

$$MSE = \frac{1}{N} \sum_{i=1}^{N} (Y(n) - T(n))^2$$

where $N$ is the size of the output vector, $Y$ is a vector of the output of the neural network, $T$ is a vector of the target values.
Based on the results in Table I, GRNN has always higher training accuracy than BP ANN and less training time. In fact, for Cholesterol and engine data set the training error for BP is very high while on the other hand for GRNN the error is very low.

In the second set of results, the output from every dataset is used to compare between GRNN and BP as shown in Fig. 4, Fig. 5, Fig. 6, Fig. 7, Fig. 8, Fig. 9, Fig. 10, and Fig. 11.

In the last part of the results, GRNN is used to control the altitude of a quadcopter model in the simulation using Matlab. The altitude tracking of the quadcopter is shown in Fig. 12. The GRNN controller is accurately follow the set point reference and the learning is quick.

## V. Conclusion

GRNN provides accurate and quick solution to regression, approximation, classification and fitting problems.

GRNN can be used in system identification of dynamic systems as well as control of dynamic systems.

GRNN outperforms BP ANNs in the accuracy and training time; however, GRNN has some limitations such as the growth of the hidden layer.

When training GRNN with a large dataset it is essential to reduce the data dimensionality using any of the data reduction techniques such as clustering or distance based algorithms.
Fig. 7. GRNN Vs BP cholesterol dataset

Fig. 8. GRNN Vs BP engine dataset

Fig. 9. GRNN Vs BP cancer dataset

Fig. 10. GRNN Vs BP iris dataset

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