Fate of stellar bars in minor merger of galaxies

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ABSTRACT
Minor merger of galaxies are common during the evolutionary phase of galaxies. Here, we investigate the dynamical impact of a minor merger (mass ratio 1:10) event on the final fate of a stellar bar in the merger remnant. To achieve that, we choose a set of minor merger models from the publicly available GalMer library of galaxy merger simulations. The models differ in terms of their orbital energy, orientation of the orbital spin vector, and morphology of the satellite galaxy (discy/spheroidal). We demonstrate that the central stellar bar, initially present in the host galaxy, undergoes a transient bar amplification phase after each pericentre passage of the satellite; in concordance with past studies of bar excitation due to tidal encounter. However, once the merger happens, the central stellar bar weakens substantially, followed by a complete destruction of the bar in merger remnant for some models. The accumulation of satellite’s stars in the central region of merger remnant plays a key role in the bar weakening/destruction process; causing a net increase in the central mass concentration as well as in the specific angular momentum content. We find that the efficiency of mass accumulation from the satellite in the central parts of merger remnants depends on the orbital parameters as well as on the satellite’s morphology. Consequently, different minor merger models display different degrees of bar weakening/destruction (partial or complete) event. This demonstrates that minor merger of galaxies is a plausible avenue for bar weakening/destruction in disc galaxies.

Key words: galaxies: elliptical and lenticular - galaxies: evolution - galaxies: formation - galaxies: halos - galaxies: kinematics and dynamics - galaxies: structure

1 INTRODUCTION
In the Lambda cold dark matter (LCDM) paradigm, galaxies grow hierarchically via major mergers and/or multiple minor mergers, and accretion of cold gas (White & Rees 1978; Fall & Efstathiou 1980). The minor merger of galaxies (mass ratio greater than or equals to 1:10) are shown to be less catastrophic than the major merger (mass ratios from 1:1 to 1:3) events, so that they can preserve the disc morphology in the post-merger remnant. However, the details of maintaining a kinematically-cold thin disc and a kinematically-hotter thick disc in the merger remnant depends on the fraction of interstellar gas present in the merging disc galaxies (e.g., see Villalobos & Helmi 2008; Moster et al. 2010). Minor mergers can happen frequently in the local Universe (e.g., see Frenk et al. 1988; Carlberg & Couchman 1989; Lacey & Cole 1993; Gao et al. 2004; Jogee et al. 2009; Kaviraj et al. 2009). Therefore, it is of key interest to understand the detailed role of minor merger of galaxies in driving the evolution of disc galaxies.

In the past, both theoretical and observational efforts have focused on the impact of minor mergers on galaxy’s evolution and reshaping their kinematics. Minor mergers are shown to leave a number of characteristic morphological finger-prints in disc galaxies (e.g., see Ibata et al. 1994, 2001; Yanny et al. 2003; Erwin et al. 2005; Ibata et al. 2005; Younger et al. 2007; Feldmann et al. 2008; Kazantzidis et al. 2009). This also causes heating of the disc and thickening the disc in the vertical direction (Quinn et al. 1993; Walker et al. 1996; Velazquez & White 1999; Font et al. 2001; Kazantzidis et al. 2008; Qu et al. 2011a), decreasing the specific angular momentum of stellar disc in the post-merger remnant, irrespective of the orbital configuration or the morphology of satellite galaxy (Qu et al. 2010, 2011b), producing inner components (such as inner ring, inner disc etc.) for unbarred galaxies (Eliche-Moral et al. 2011), enhancing star formation activities (e.g., see Kaviraj 2014), and radially distributing the chemical abundances in Milky Way-like galaxies (e.g., see

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Past observations have shown that about two-third of the disc galaxies in the local universe host bars (e.g., see Eskridge et al. 2000; Whyte et al. 2002; Aguerri et al. 2009; Masters et al. 2011). The occurrence of bars is found to depend strongly on the stellar mass (e.g., Nair & Abraham 2010), Hubble type (e.g., Aguerri et al. 2009; Buta et al. 2010; Nair & Abraham 2010) of the host galaxies. Whether the remaining one-third of disc galaxies in the local Universe are hostile to the bar formation and their growth, or the bar has been destroyed during their evolutionary trajectory – it is still not completely understood (Saha & Elmegreen 2018).

Destroying completely a central stellar bar has proven to be an arduous task. Past theoretical studies have identified central mass concentration and inflow of gas as plausible mechanisms for bar destruction; however it might require prodigious amount of gas inflow or a very high central mass concentration (e.g., see Pfenniger & Norman 1990; Shen & Sellwood 2004; Athanassoula et al. 2005; Bournaud et al. 2005; Hoizumi & Hernquist 2005; Athanassoula et al. 2013). Also, recent observational work by Palwa & Saha (2018) showed the presence of prominent bar in several low-surface-brightness (LSB) galaxies with high gas fraction. The bar fraction in the high-redshift galaxies is still debated; some studies claimed a decreasing bar fraction with increasing redshift (e.g., see Sheth et al. 2008; Melvin et al. 2014; Simmons et al. 2014), while some other studies showed a constant bar fraction up to redshift $z \sim 1$ (e.g., Elmegreen et al. 2004; Jogee et al. 2004). Nevertheless, this large abundance of stellar bars in disc galaxies and the relatively larger frequency of occurrence of minor merger events (e.g., Fakhouri & Ma 2008) of disc galaxies raises an important question – what happens to a stellar bar when the host galaxy experiences a minor merger event with a satellite galaxy?

Past studies have focused on the dynamical effect of tidal encounter in triggering the bar instability in disc galaxies. The increased bar fraction in the central regions of Virgo and and Coma cluster suggested that tidal interactions can trigger bar formation in disc galaxies, especially in the Early-type disc galaxies (e.g., see Thompson 1981; Guiricin et al. 1993; Andersen 1996; Barazza et al. 2009; Méndez-Abreu et al. 2012; Lin et al. 2014). Later observational studies indicated that bar formation due to a fly-by encounter depends on the galaxy’s mass and their ability to maintain a cold disc component against the heating caused the tidal encounter (e.g., Méndez-Abreu et al. 2012). Bar formation due to a tidal encounter and its effect on the bar properties has been further studied extensively using N-body simulation of disc galaxies (e.g., see Noguchi 1987; Gerin et al. 1990; Sundin et al. 1993; Miwa & Noguchi 1998; Aguerri & González-García 2009; Peirani et al. 2009; Lang et al. 2014; Martínez-Valpuesta et al. 2017). Additionally, the properties of the resulting bar are shown to depend on the presence of the interstellar gas (e.g., Berentzen et al. 2003), mass ratio of the galaxies, and/or the relative phase of the bar and the companion at pericentre (e.g., see Gerin et al. 1990; Sundin et al. 1993; Lang et al. 2014; Lokas et al. 2014). Despite a significant research in the field, the exact dynamical role of minor mergers on the final fate of a stellar bar remains to be explored. This is particularly true when the companion/satellite galaxy ultimately plunges into the host galaxy and the host galaxy readjusts after the merger is completed. The exact role of different orbital parameters, Hubble type of companion, gas fraction in disc galaxy is not known either in context of reshaping the $m = 2$ bar mode during a minor merger event.

In this paper, we carry out a systematic study of the temporal evolution of bar properties and the associated disc kinematics during a minor merger event while varying different orbital parameters, nature of satellite galaxies. For this, we make use of the publicly available minor merger simulation models from the GalMer database (Chilingarian et al. 2010). The GalMer library offers to study the physical effects of minor merger process, encompassing a wide range of cosmologically motivated initial conditions; thus, it is well-suited for the goal of this paper.

The rest of the paper is organised as follows: Section 2 provides the details of minor merger models used here while Section 3 quantifies the temporal change of stellar bar in minor mergers. Section 4 provides the details of underlying physical mechanisms liable for bar weakening/destruction. Section 5 discusses the dependence on the morphology of the satellite galaxy. Sections 6 and 7 contain discussion and the main findings of this work, respectively.

2 MODELS OF MINOR MERGERS – GALMER DATABASE

GalMer is a publicly available library of N-body+smooth particle hydrodynamics (SPH) simulation of galaxy mergers to probe the details of galaxy formation through hierarchical merger process. The morphology of galaxy models ranges from ellipticals to late-type, gas-rich spirals. A galaxy model consists of a non-rotating spherical dark matter halo, a stellar and a gaseous disc (optional), and a central non-rotating bulge (optional). The dark matter halo and the central bulge (if present) are modelled as Plummer sphere (Plummer 1911) whereas the stellar and the gaseous disc are modelled as Miyamoto-Nagai density profiles (Miyamoto & Nagai 1975).

The GalMer library offers three different galaxy interaction/merger scenarios, namely, the giant-giant major merger (mass ratio of $1:1$), giant-intermediate merger (mass ratio of $1:2$), and the giant-dwarf minor merger (mass ratio of $1:10$). The total number of particles ($N_{\text{tot}}$) varies from giant-giant interaction ($N_{\text{tot}} = 120,000$) to giant-dwarf interaction ($N_{\text{tot}} = 480,000$). Gas particles in the simulation are treated as ‘hybrid particles’, and are characterised by two masses, namely, the gravitational mass (remaining fixed during simulation), and the gas mass (changing with time) denoting the gas content of the particles (for details see Chilingarian et al. 2010).

The orientation of each galaxy in the orbital plane is characterised by the spherical coordinates, $i_1, i_2, \Phi_1$, and $\Phi_2$ (for details, see fig. 3 of Chilingarian et al. 2010). A suitable empirical relation to follow the star formation process is implemented so as to reproduce the observed Schmidt law for the interacting galaxies. The simulation models also include
the recipes for the (gas phase) metallicity evolution as well as the supernova feedback. The merger simulations are evolved using a TreeSPH code by Semelin & Combes (2002). The galaxy models are evolved in isolation for 1 Gyr before the start of merger simulation (Chilingarian et al. 2010). Here, we consider a set of giant-dwarf minor merger models where the host galaxy is of Sa-type and the morphology of the satellite galaxy varies from dE0 to dSb. GalMer provides only one orbital configuration for the giant-dwarf interaction, characterised by $i_1 = 33^\circ$ and $i_2 = 130^\circ$ (Chilingarian et al. 2010). Each minor merger model is referred to as a unique string given by ‘[host galaxy][satellite galaxy][orbit ID][orbital spin]’ where [host galaxy] and [satellite galaxy] denote their morphology types, and [orbit ID] denotes the orbital number as assigned in the GalMer library. [orbital spin] denotes the orbital spin vector (‘dir’ for direct and ‘ret’ for retrograde orbits), and ‘33’ refers to $i_1 = 33^\circ$. We follow this scheme of nomenclature throughout the paper. The key orbital parameters of the minor merger models considered here, are listed in Table 1. We define the epoch of merger, $T_{\text{merge}}$, when the distance between the centre of mass of two galaxies becomes close to zero. The resulting $T_{\text{merge}}$, along with the times of first and second pericentre passages for the selected minor merger models are also listed in Table 1.

3 FATE OF STELLAR BARS IN MINOR MERGERS

Here, we investigate how a central stellar bar in a host galaxy evolves after it suffers a minor merger (mass ratio 1:10) with a satellite galaxy. To do that, we choose a minor merger model gSadE001dir33 from the GalMer database where a dwarf E0-type galaxy merges with a host giant Sa-type galaxy. In the beginning, the host galaxy (gSa) harbours a prominent central stellar bar; thereby serving an ideal testbed for this work. Fig. 1 shows the temporal evolution of distance between the centres of mass of these two galaxies. After each pericentre passage, the satellite loses a fraction of its orbital angular momentum due to the dynamical friction and the tidal torque. Consequently, it falls deep in the gravitational potential of the host galaxy and ultimately merges with the host galaxy. Fig. 2 shows the face-on density distribution of stellar particles of the minor merger model gSadE001dir33 at six different epochs, before and after the merger. At the beginning ($t = 0$ Gyr), the host (gSa) galaxy harbours a prominent stellar bar as delineated by the central elongated contours; however, at the end of the simulation ($t = 3.8$ Gyr), the contours in the central region of the merger remnant are rounded in shape, suggestive of the bar weakening phenomenon.

To probe further, we created the face-on density maps at the beginning and at the end of the model gSadE001dir33, and performed a multi-component decomposition of the radial density profiles. The radial profiles of surface density, the ellipticity ($\epsilon = 1 - b/a$, $a$ and $b$ being semi-major and semi-minor axes, respectively) and the position angle (PA) are obtained by using IRAF ELLIPSE task. The extracted radial density profiles are then decomposed into disc+bulge or disc+bulge+bar (when the bar is present). The bulge is represented by a Sérsic profile with Sérsic index $n_1$, effective radius $R_{e1}$ and effective surface density $I_{e1}$. The disc is modelled with an exponential profile with central surface density $I_{00}$ and disk scale-length $R_d$. Additionally, when a bar is present, it is represented by another Sérsic profile with Sérsic index $n_2$, effective radius $R_{e2}$, and effective surface density $I_{e2}$ (Elmegreen et al. 1996). Mathematically, all the components can be represented as:

$$I(R) = I_0 e^{-(R/R_d)} + I_{e1} e^{-b_n [(R/R_{e1})^{1/(n_1)} - 1]} + I_{e2} e^{-b_n [(R/R_{e2})^{1/(n_2)} - 1]},$$

where the multi-component fitting has been performed with PROFILER software (Ciambrú 2016).

Fig. 3 shows the multi-component decomposition of radial surface density at the start ($t = 0$ Gyr) and the end of the simulation run ($t = 3.8$ Gyr), along with the corresponding radial profiles of the ellipticity ($\epsilon$) and the position angle (PA). The presence of a second Sérsic component (with $n_2 = 0.47$, and $R_{e2} = 2.53$ kpc) at $t = 0$ clearly demonstrates the presence of bar. This is further supported by a characteristic peak in the radial ellipticity ($\epsilon$) profile ($\epsilon_{\text{max}} \sim 0.56$) and constant position angle (PA) values in the central bar region. However, at the end of the simulation run ($t = 3.8$ Gyr), the final morphology resembles an S0 galaxy with no discernible central bar; the peak value of the ellipticity ($\epsilon_{\text{max}}$) reduces to 0.14 at $t = 3.8$ Gyr.

To quantify the temporal change of the central stellar bar, we calculated the radial profiles of $m = 2$ and $m = 4$ Fourier components ($A_2/A_0$ and $A_4/A_0$), at the beginning and at the end of the simulation gSadE001dir33. This is shown in Fig. 4 (top panel). At the beginning, the presence of the bar is clearly indicated by a peak in the radial profile of $m = 2$ Fourier component in the central region; however, at $t = 3.8$ Gyr, the peak value of the radial profile of $m = 2$ Fourier coefficient is well below 0.2, indicating the bar has been destroyed (Saha & Naab 2013). Also, at $t = 3.8$ Gyr, the peak value of $m = 4$ Fourier coefficient is small. We define the strength of the bar, $S_{\text{bar}}$, at any given time $t$, as $S_{\text{bar}} = (A_2/A_0)_{\text{max}}$, where $A_m$ is the coefficient of $m$th Fourier harmonics. Fig. 4 (bottom panel) shows the corresponding temporal evolution of bar strength. After each pericentre passage, the initial bar gets stronger due to the tidal inter-
Table 1. Key parameters for the selected minor merger models from GalMer library

| model                  | \(r_{\text{ini}}\) (kpc) | \(v_{\text{ini}}\) (\(\times 10^2\) km s\(^{-1}\)) | \(L_{\text{ini}}\) (\(\times 10^4\) km\(^2\) s\(^{-2}\)) | \(E_{\text{ini}}\) (\(\times 10^2\) km\(^2\) s\(^{-2}\)) | \(\text{spin}\) | \(T_{1,\text{peri}}\) (Gyr) | \(T_{2,\text{peri}}\) (Gyr) | \(T_{\text{merger}}\) (Gyr) | \(T_{\text{end}}\) (Gyr) |
|------------------------|--------------------------|----------------------------------|----------------------------------|--------------------------|----------------|---------------------|---------------------|------------------|----------------|
| gSadE001dir33          | 100                      | 1.48                             | 29.66                            | 0.0                       | up             | 8.0                 | 1.1                 | 1.55             | 3.8             |
| gSadE001ret33          | 100                      | 1.48                             | 29.66                            | 0.0                       | down           | 8.0                 | 1.3                 | 1.95             | 3.8             |
| gSadE002dir33          | 100                      | 1.52                             | 29.69                            | 0.05                      | up             | 8.0                 | 1.4                 | 1.55             | 3.0             |
| gSadE002ret33          | 100                      | 1.52                             | 29.69                            | 0.05                      | down           | 8.0                 | 1.4                 | 2.5              | 3.0             |
| gSadE003dir33          | 100                      | 1.55                             | 29.72                            | 0.1                       | up             | 8.0                 | 1.4                 | 1.95             | 3.0             |
| gSadE003ret33          | 100                      | 1.55                             | 29.72                            | 0.1                       | down           | 8.0                 | 1.4                 | 2.5              | 3.0             |
| gSadE004dir33          | 100                      | 1.48                             | 36.33                            | 0.0                       | up             | 8.0                 | 1.2                 | 1.7              | 3.0             |
| gSadE004ret33          | 100                      | 1.48                             | 36.33                            | 0.0                       | down           | 8.0                 | 1.75                | 2.85             | 3.0             |
| gSadE006dir33          | 100                      | 1.55                             | 36.43                            | 0.1                       | up             | 16.0                | 1.45                | 2.5              | 3.0             |
| gSadE006ret33          | 100                      | 1.55                             | 36.43                            | 0.1                       | down           | 16.0                | 1.95                | 2.85             | 3.0             |
| gSadSb01dir33          | 100                      | 1.48                             | 29.66                            | 0.0                       | up             | 8.0                 | 1.45                | 1.85             | 3.0             |
| gSadSb01ret33          | 100                      | 1.48                             | 29.66                            | 0.0                       | down           | 8.0                 | 1.45                | 1.85             | 3.0             |

(1) GalMer minor merger model; (2) initial separation between two galaxies; (3) absolute value of initial relative velocity; (4) \(L_{\text{ini}} = |r_{\text{ini}} \times v_{\text{ini}}|\); (5) \(E_{\text{ini}} = v_{\text{ini}}^2 - G(m_1 + m_2)/r_{\text{ini}}\), with \(m_1 = 2.3 \times 10^{11} M_\odot\), and \(m_2 = 2.3 \times 10^{10} M_\odot\); (6) orbital spin; (7) pericentre distance; (8) epoch of first pericentre passage; (9) epoch of second pericentre passage; (10) epoch of merger; (11) total simulation run time.

Columns (2)-(7) are taken from Chilingarian et al. (2010).

Figure 2. Top panels: Face-on density distribution of host plus satellite (gSa+dE0) system, shown at different epochs for the minor merger model gSadE001dir33. The rectangular boxes (in maroon) delineate the central 20 kpc × 20 kpc region which includes the initial bar region. Bottom panels: zoom-in view of the central 20 kpc × 20 kpc region. Black lines denote the contours of constant surface density.

action, as indicated by the peaks in the \(S_{\text{bar}}\) (compare Figs 4 and 2). This is in accordance with what has been shown previously where a bar instability can be excited in a tidal interaction (e.g., Peirani et al. 2009; Lang et al. 2014; Lokas et al. 2014; Martinez-Valpuesta et al. 2017, and references in section 1). However, after the satellite merges with the host galaxy, the bar strength decays steadily; at the end of the simulation \((t = 3.8\text{ Gyr})\), the value of \(S_{\text{bar}}\) is well below 0.2, thereby conclusively demonstrating the destruction of the central stellar bar in the post-merger remnant of a minor merger.

3.1 Dependence on orbital parameters

Here we explore different minor merger models with different orbital energies and orientation of the orbital spin vectors (prograde/retrograde). To do that, we choose minor merger models with higher orbit numbers from the GalMer library.
For these models, the orbital energies are higher than that for the gSadE001dir33 model (for details see section 2). Fig. 5 (top panel) shows the time evolution of distance between centres of mass of two galaxies for different orbital configurations considered here. We point out that the time of interaction, i.e., the time interval between the first pericentre passage and the time of merging (Tmerge), gets systematically enhanced as orbital energies are increased. This trend is much more pronounced when compared between a direct and a retrograde orbital configuration having same orbital energy.

We now investigate how the temporal evolution of central bar in a minor merger scenario depends on orbital energies and orientation of the orbital spin vectors. First, we performed the multi-component decomposition of the radial surface density profiles (as outlined in section 3) at the end of the simulation runs for all minor merger models considered here. However, for the sake of brevity, these are not shown here. We noticed that, for some minor merger models, the central bar is not destroyed completely by the end of the simulation run; a second Sérsic profile (representing the bar) has to be used to achieve a reasonable best-fit model of the radial surface density. However, for those minor merger models where the bar is not destroyed completely, the resulting Sérsic ‘n’ for bar is less than 0.47 (Sérsic ‘n’ for bar obtained at $t = 0$, see Fig. 3). This implies that the mass distribution of the central $m = 2$ non-axisymmetric structure gets more flattened by the end of the simulation run. Also, the peak in the radial ellipticity profile ($e_{\text{max}}$) is diminished from its initial value ($e_{\text{max}} \sim 0.36$ at $t = 0$ Gyr); thus, further supporting the fact that the central non-axisymmetric structure has become rounder by the end of the simulation run.

Next, we probe the dependence of the temporal evolution of the bar strength, $S_{\text{bar}}$, on different orbital energies and orientation of the orbital spin vectors. This is shown in Fig. 5 (bottom panel). We found that in all minor merger models considered here, each pericenter passage of the satellite produces a transient increase in the bar strength ($S_{\text{bar}}$); a scenario similar to the case of gSadE001dir33 model. This finding is at par with the past studies which demonstrated the triggering of bar mode in disc galaxies due to the tidal encounter (e.g., Peirani et al. 2009; Lang et al. 2014; Lokas et al. 2014; Martinez-Valpuesta et al. 2017). However, once the satellite merges with the host galaxy, the bar strength decreases steadily. In some cases, the value of $S_{\text{bar}}$ at the end of the simulation run ($t = 3$ Gyr) is still higher than 0.2. This shows that for those models, the bar is not completely destroyed; rather weakened. Nevertheless, the steady decreasing trend of $S_{\text{bar}}$ implies that if these models were evolved for another $0.5 - 1$ Gyr, the bar in the merger remnant would have been completely destroyed. This shows that the bar weakening phenomenon, with bar getting destroyed in some occasions, in minor merger event is a generic process, irre-
Here, we investigate how the mass concentration in the central region (encompassing the bar) changes with time, before and after the minor merger occurs.

Fig. 6 (top panel) shows the radial mass distribution at the beginning and at the end ($t = 3.8$ Gyr) of the minor merger model gSadE001dir33. We calculated the radial mass profiles, first considering only the stellar particles from the host galaxy, and then, taking all the stellar particles from both the host and the satellite galaxy. This scheme, in turn, will reveal the relative contribution of the host and the satellite galaxy separately in the net mass change within the central bar region. Fig. 6 reveals that the initial, centrally-concentrated stellar particles of the host galaxy is dispersed at larger radii at later epochs. This in turn, leads to a decrease in the total mass of the central bar region, and a flattened mass distribution at larger radii from the centre. However, when the stellar particles of both the host and satellite galaxies are considered, the radial mass distribution, at $t = 3.8$ Gyr, displays a net mass enhancement in the central bar region. This shows the accumulation of stellar particles from the satellite galaxy is liable for the net mass increment within the bar region.

Next, we probe in details the distribution of accumulated stellar particles from the satellite in the central bar region. Fig. 7 further demonstrates the steady accumulation of satellite’s particles within the central bar region. We point out that, the accumulated stellar particles from the satellite are not aligned preferentially in the disc plane; rather they are distributed over the whole bar region, and the distribution is vertically extended. Even for a direct orbital configuration, the angle of inclination is not zero ($i_1 = 33^\circ$, see section 2), which in turn prevents the accumulated particles to be aligned in the disc plane. These accumulated stellar particles from the satellite galaxy is liable for the net mass change in the central region (encompassing the bar) changes with time, before and after the minor merger occurs.

In the previous sections, we demonstrated that a minor merger leads to a steady decrease in the bar strength implying the bar weakening event. This trend holds true for different orbital parameters (e.g., orbital energy, orientation of orbital spin vector). Here we explore the underlying physical mechanisms which are liable for the bar weakening.

### 4 PHYSICAL CAUSE OF BAR WEAKENING

In the previous sections, we demonstrated that a minor merger leads to a steady decrease in the bar strength implying the bar weakening event. This trend holds true for different orbital parameters (e.g., orbital energy, orientation of orbital spin vector). Here we explore the underlying physical mechanisms which are liable for the bar weakening.

#### 4.1 Central mass enhancement

Past theoretical studies showed that a massive central mass concentration can destroy/weaken a stellar bar. However, this process might require a very high central mass content (~5 per cent of the disc mass, see e.g., Shen & Sellwood 2004; Athanassoula et al. 2005; Hozumi & Hernquist 2005).

Figure 5. Top panel shows the distance between the centres of the satellite (dE0) and the host galaxy (gSa) as a function of time, for different orbital configurations (for details see section 3.1). Bottom panel shows the temporal evolution of the bar strength, $S_{bar}$ for a few orbits with different orbital energies and orbital spin orientations (dir/retrograde). Solid and dashed lines denote direct and retrograde orbits, respectively.

![Figure 5](https://example.com/figure5.png)

**Figure 5.** Top panel shows the distance between the centres of the satellite (dE0) and the host galaxy (gSa) as a function of time, for different orbital configurations (for details see section 3.1). Bottom panel shows the temporal evolution of the bar strength, $S_{bar}$ for a few orbits with different orbital energies and orbital spin orientations (dir/retrograde). Solid and dashed lines denote direct and retrograde orbits, respectively.

Figure 6. Radial mass distribution, calculated at the beginning and at the end ($t = 3.8$ Gyr) of the simulation run for the model gSadE001dir33. Blue dashed line denotes the contribution from the host (gSa) galaxy whereas red dashed line shows for the host plus satellite (gSa+dE0) system. The central bar region ($R \leq 6.1$ kpc as indicated within the green box) is shown in the inset. The mass is in units of $2.25 \times 10^9 M_\odot$.

![Figure 6](https://example.com/figure6.png)
particles from the satellite participates in forming a thick-disc in the post-merger remnant (Qu et al. 2011a,b). The physical implication of this accumulation process in context of the bar weakening process is discussed later.

Finally, we calculated the temporal evolution of the mass increase within the bar region. We measure that, at $t = 0$, the central bar extent ($R_{\text{bar}}$) is $\sim 6.1$ kpc. For uniform comparison, we kept the extent of the bar region fixed at 6.1 kpc at later time-steps. We checked that the bar extent varies less than 20 per cent of its initial extent during the entire ‘bar phase’, and therefore would not introduce any artefact in the subsequent analyses. Fig. 8 shows the corresponding temporal evolution of the change in the central mass content within the bar region ($\Delta M_{\text{bar}}(t; R < R_{\text{bar}})$, defined in Eq.2), for different minor merger models considered here. The net change in the mass within the bar region for the host plus satellite system is given as

$$\Delta M_{\text{net}}(t; R < R_{\text{bar}}) = \Delta M_{\text{host}}(t; R < R_{\text{bar}}) + \Delta M_{\text{sat}}(t; R < R_{\text{bar}})$$

where $\Delta M_{\text{host}}$, and $\Delta M_{\text{sat}}$ are the contributions from the host and the satellite galaxy, respectively; they are calculated as

$$\Delta M(t; R < R_{\text{bar}}) = M(t; R < R_{\text{bar}}) - M(t = 0; R < R_{\text{bar}}).$$

Fig. 8 brings out the fact that $\Delta M_{\text{host}}$ and $\Delta M_{\text{sat}}$ have an opposite effect within the bar region. The mass fraction of the stellar particles of host galaxy decreases with respect to the initial epoch. However, after the merger happens, a fraction of stellar particles of the satellite galaxy gets trapped within the bar region (as also shown in Fig. 7). Hence, the net change in mass fraction within the bar region will be determined by the dominant of these two opposite effects of the host and the satellite galaxies. Fig. 8 shows the general trend that, within the bar region, the mass accumulation from the satellite galaxy always dominates over the instantaneous mass loss from the host galaxy. This trend holds for the dE0-type satellite galaxy, and for different orbital energies and the orientation of the orbital spin vectors considered here.

Here, we briefly compare the bar weakening by mass accumulation scenario during the minor mergers with the past literature of bar weakening via growth of central mass concentration (hereafter CMC). We note that, the mass accumulation within the central bar region varies from $3.1 \times 10^9 \, M_\odot$ to $4.6 \times 10^9 \, M_\odot$ (equivalently, $\sim 3 - 4$ per cent of the total stellar mass of the host galaxy) for the direct orbits. Similarly, for retrograde orbits, the mass accumulation within the central bar region varies from $4 \times 10^9 \, M_\odot$ to $5.75 \times 10^9 \, M_\odot$ (equivalently, $\sim 3.5 - 5$ per cent of the total stellar mass of the host galaxy). Past studies on bar destruction/weakening by CMC quoted the required mass to be $\sim 5$ per cent of the disc mass (e.g., see Shen & Sellwood 2004; Athanassoula et al. 2005; Hozumi & Hernquist 2005). Therefore, the amount of mass accumulation seen in our minor merger models is within the estimated range as reported in the past literature.

Also, we point out that in past numerical simulations, the CMCs were introduced in an adiabatic fashion. The time for full growth of CMC ($t_{\text{grow}}$) varies from 0.7-1.5 Gyr (e.g., see Shen & Sellwood 2004; Athanassoula et al. 2005; Hozumi & Hernquist 2005). Thus, the (simulated) galaxy could readjust itself to the secular change of the underlying potential. On the other hand, in our selected minor merger models, the mass accumulation in the central bar region happens in a rather short time-span after the merger happens ($\sim 150 - 250 \, \text{Myr}$). Thus, the merger remnant could not readjust itself to the abrupt change in the underlying potential.

### 4.2 Angular momentum exchange

Past studies have demonstrated that a bar can grow in amplitudes by transferring the disc angular momentum to the dark matter halo; this transfer takes place at the bar resonances (e.g., see Tremaine & Weinberg 1984; Hernquist & Weinberg 1992; Debattista & Sellwood 2000; Athanassoula 2002; Sellwood & Debattista 2006; Dubinski et al. 2009; Saha & Naab 2013). On the other hand, Bournaud et al. (2005) showed that the angular momentum transfer, from the gas inflow to the stellar bar, can potentially weaken the
bar. Here, we study in detail the angular momentum exchange during a minor merger event. During a minor merger event, the orbital angular momentum is distributed in both the host and the satellite galaxies where the satellite always gains a part of the orbital angular momentum, irrespective of orbital energy, and orientation (for details see Qu et al. 2010). The detailed redistribution of internal angular momentum into different components, namely, disc, bulge, and dark matter (hereafter DM) halo of the host galaxy is shown in Appendix A.

Here, we focus on the central bar region \((R < R_{\text{bar}})\) and study in detail the temporal evolution of angular momentum (hereafter AM) within the bar region during the bar weakening/destruction process. As in section 4.1, we keep the extent of the bar region fixed at 6.1 kpc while measuring the change in the specific AM. At time \(t\), we calculate the \(z\)-component of the specific AM of the stellar particles of the host or the satellite galaxy, within the bar region using the definition

\[
l_z(t; R < R_{\text{bar}}) = \frac{1}{N(t)} \sum_{i=1}^{N(t)} \left[ x_i(t)v_y(t) - y_i(t)v_x(t) \right],
\]

(4)

where \(N(t)\) is the total number of stellar particles contained within the bar region at time \(t\), and \(x, y, v_x, v_y\) are the position and velocity of the particles. The corresponding change in the internal specific AM is calculated as

\[
\Delta l_z(t; R < R_{\text{bar}}) = l_z(t; R < R_{\text{bar}}) - l_z(t = 0; R < R_{\text{bar}}).
\]

(5)
However, the change in the specific AM within the bar region due to the host plus satellite system is calculated, using the definition of total differential, as

$$\Delta l_{z,\text{net}}(t; R < R_{\text{bar}}) = l_{z,\text{net}}(t; R < R_{\text{bar}}) \times \left[ \frac{\Delta l_{z,\text{net}}(t; R < R_{\text{bar}})}{l_{z,\text{net}}(t)} - \frac{\Delta M_{\text{net}}(t; R < R_{\text{bar}})}{M_{\text{net}}(t; R < R_{\text{bar}})} \right]$$

(6)

where $l_z(t; R < R_{\text{bar}})$ is the $z$-component of the AM within the bar region at time $t$. The subscript ‘net’ denotes the quantities that are calculated by taking into account the stellar particles from both the host and the satellite galaxies within the bar region. We caution that for calculating $\Delta l_{z,\text{net}}(t; R < R_{\text{bar}})$, the individual change of specific AM from the host and the satellite galaxies cannot be simply co-added (unlike the case of $\Delta M_{\text{net}}(t; R < R_{\text{bar}})$), and has to be calculated using Eq. 6.

Fig. 9 shows the temporal evolution of the change in the specific AM content within the bar region, for different minor merger models. The specific AM of the host galaxy within the bar region decreases with time, and this holds true for both the direct and retrograde orbital configurations. However, the specific AM loss within the bar region due to the host galaxy alone is more for a direct orbit than for a retrograde orbit with same orbital energy (compare top and bottom panels of Fig. 9). We checked that, the stellar particles from the satellite galaxy which eventually get trapped within the central bar region, contain high specific AM; thereby bringing in specific AM within the bar region. The net loss of specific AM within the bar region for the host plus satellite system is thus less when compared to the specific AM loss from the host galaxy alone. In other words, some fraction of specific AM loss due to the host galaxy is compensated by the fresh addition of stellar particles from the satellite galaxy having high specific AM.

Finally, Fig. 10 compares the joint effects of temporal mass change and the specific AM change within the bar region, for different minor merger models. For the direct orbits with increasing orbital energy, the mass increase is progressively less, as reflected in the lesser values of $\Delta M_{\text{net}}(t; R < R_{\text{bar}})$. Also, the loss in specific AM within the bar region is progressively more with increasing orbital energy. These together cause progressively lesser degree of bar weakening. However, for retrograde orbits, the trend is seen to differ from the direct orbits. For retrograde orbits, both the mass increase and the loss in specific AM within the bar region is progressively more with increasing orbital energy. The physical reason is as follows. The mass loss within the bar region due to the host galaxy is more for a direct orbit when compared with a retrograde orbit with same orbital energy. However, the fraction of mass accumulated within the bar region from the satellite remains similar for a direct and a retrograde orbit (with same orbital energy). This gives rise to the different behaviour in the temporal mass increment for direct and retrograde orbits.

To conclude, a minor merger event can be a plausible scenario for bar weakening/destruction. The efficiency of the bar weakening/destruction process during a minor merger event relies on the effectively bringing of the stellar particles from the satellite galaxy within the bar region. The time-interval of mass accumulation (abrupt versus adiabatic) also plays a pivotal role in disrupting the ordered periodic orbits ($x_1$- and $x_2$- families) which serve as a backbone of the stellar bar. The vertically extended distribution (as opposed to aligned in disc plane) of accumulated particles from the satellite, with different kinematics as the previous host’s disc particles, prevents the sustainability of the bar.

5 Dependence on morphology of satellite galaxy

So far, we have considered minor merger scenarios where the satellite galaxy is a dwarf E0 galaxy. Here, we study the efficiency of the bar weakening/destruction process when the satellite galaxy has a disc morphology. For this, we consider here two minor merger models from GaMer database where the satellite galaxy is of dwarf Sb-type. Fig. 11 (top panels) show temporal evolution of distance between the centres of mass of these two galaxies and the associated temporal evolution of the bar strength ($S_{\text{bar}}$). In both the cases, the bar weakens after the merging happens. However, the degree of bar weakening is different for direct and retrograde orbital configurations. The bar in the direct orbits gets completely destroyed by the end of the simulation run ($S_{\text{bar}} < 0.2$) whereas for the retrograde orbit, bar is still not completely destroyed ($S_{\text{bar}} \sim 0.2$).

Fig. 11 (bottom panel) also brings out the different scenarios of mass accumulation of stellar particles from the satellite galaxy within the bar region. We then quantified the temporal change in the mass and the specific AM content within the bar region for these two models. This is shown in Fig. 12. The mass accumulation from the satellite within the bar region is less for the retrograde orbit than in direct orbit case. Note that the merger occurs at a later epoch for the retrograde case when compared with the direct orbit. Hence, by the end of simulation run ($t = 3 \text{ Gyr}$), the merger remnant for the retrograde orbit, did not get much time to readjust fully. Also, the addition of satellite’s stellar particles (with high specific AM) compensates a part of specific of AM loss due to the host galaxy, within the bar region. This trend is similar to the minor merger models with spheroidal satellite galaxy. However, as the fraction of stellar particles from the satellite galaxy within the bar region is small for the retrograde orbit than the direct orbit, the net change in specific AM for the host plus satellite system closely follow that for the host galaxy.

In the previous sections, the mass accumulation and gain in specific AM in the central bar region are shown to play key roles in the bar weakening/destruction. Next, we compare how these processes vary with the morphology of satellite galaxy (discy versus spheroidal). We find that, for the same orbital configuration, the mass accumulation process in the central part from the satellite is more efficient for a spheroidal satellite as compared to a discy satellite galaxy. This happens because for a given orbit, a satellite with higher central concentration is less resistive to the tidal effect of the host galaxy. Consequently it decays rapidly in the central part of the host galaxy. The variation in accumulated mass fraction with satellite’s morphology affects the change in specific AM as well, within the bar region. When the orbital parameters are kept fixed, the gain of specific AM within the central bar region due to the satellite’s is lesser for a discy satellite than a spheroidal satellite. Therefore, the
Figure 9. Change of $z$-component of specific angular momentum, $\Delta l_z(t; R < R_{\text{bar}})$, averaged within the initial bar region ($R \leq 6.1$ kpc), shown as a function of time, for different GalMer minor merger models. The averaging is done while taking the stellar particles from host (gSa), and host plus satellite galaxies (red and blue lines), respectively. $\Delta l_z(t; R < R_{\text{bar}})$ is normalised by the $z$-component of specific angular momentum of all stellar particles of the host galaxy at $t = 0$. Vertical arrows (in magenta) indicate the epochs of first and second pericentre passages and the epoch of merger, respectively.

net change in specific AM for the host plus satellite system close follow the evolution of specific AM for the host galaxy. This further outlines the importance of effectively bringing the stellar particles from the satellite galaxy within the bar region on the efficiency of the bar weakening process.

6 DISCUSSION

6.1 Case of a delayed merger scenario

Here we consider a scenario of delayed minor merger and study the temporal evolution of the bar properties in the host galaxy. To do that, we considered two minor merger models from the GalMer library for which the merger happens at a very later epoch. Thus, these models mimic the sce-
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6.2 Bar fraction and gas accretion

In most of the cases explored here, the satellite or the perturber galaxy merges with the host galaxy; the typical timescale for the merger to happen is around 2 Gyr after the start of the simulation run. We showed that an initial bar weakens or in some cases, are completely destroyed after the merger is completed. Since minor mergers are common in the local Universe (e.g., see Frenk et al. 1988; Carlberg & Couchman 1989; Lacey & Cole 1993; Gao et al. 2004; Fakhouri & Ma 2008; Jogee et al. 2009; Kaviraj et al. 2009), therefore the findings of this paper is in apparent tension with the high frequency of the bar incidence in nearby galaxies. In addition, a galaxy might undergo multiple minor merger events during their entire lifetime (e.g., see Hopkins et al. 2009); thus, making the bar weakening/destruction event more inevitable. However, in reality, the situation is different as a galaxy might be accreting cold gas (e.g., Birnboim & Dekel 2003; Kereš et al. 2005; Dekel & Birnboim 2006; Ocvirk et al. 2008; Cornuault et al. 2018) either during the mergers or at a later stage and this in turn could rejuvenate the bar (e.g., see Semelin & Combes 2002; Bournaud et al. 2005; Combes 2008; Marino et al. 2011). Indeed, recent observational studies have pointed out such indication of bar rejuvenation event (e.g. Barway & Saha 2020). Hence, the bar weakening/destruction scenario during a minor merger...
event as shown in this paper is more appropriate for early-type disc galaxies which are in general gas poor (e.g., Young & Scoville 1991). The fraction of galaxies hosting bars decreases from the late-type gas-rich disc galaxies to early-type gas-poor disc galaxies (e.g. see Nair & Abraham 2010). The bar fraction in disc galaxies tend to reach their minimum values for the lenticular/S0 galaxies (e.g., see Aguerri et al. 2009; Buta et al. 2010; Nair & Abraham 2010; Barway et al. 2011). The absence of bar in the early-type galaxies thus can be attributed to recent minor merger events which are dry to a large extent.

7 CONCLUSION

In summary, we investigated the dynamical impact of minor merger of galaxies (mass ratio 1:10) on the survival of a stellar bar, initially present in the host galaxy. We selected a set of minor merger models, with varying orbital energy, orientation of orbital spin vector, morphology of satellite galaxy from the publicly available GalMer library of galaxy merger simulations which is a part of HORIZON project (http://www.projet-horizon.fr/rubrique3.html).

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DATA AVAILABILITY

The simulation data of minor merger models used here is publicly available from the URL http://galmer.obspm.fr.

REFERENCES

Aguerri J. A. L., González-García A. C., 2009, A&A, 494, 891
Aguerri J. A. L., Méndez-Abreu J., Corsini E. M., 2009, A&A, 495, 491
Andersen V., 1996, AJ, 111, 1805
Athanassoula E., 2002, ApJ, 569, L83
Athanassoula E., Lambert J. C., Dehnen W., 2005, MNRAS, 363, 496
Athanassoula E., Machado R. E. G., Rodionov S. A., 2013, MNRAS, 429, 1949
Barazza F. D., et al., 2009, A&A, 497, 713
Barway S., Saha K., 2020, MNRAS, 495, 4548
Barway S., Wadadekar Y., Kembhavi A. K., 2011, MNRAS, 410, L18
Berentzen I., Athanassoula E., Heller C. H., Fricke K. J., 2003, MNRAS, 341, 343
Birnboim Y., Dekel A., 2003, MNRAS, 345, 349
Bournaud F., Combes F., Semelin B., 2005, MNRAS, 364, L18
Buta R., Laurikainen E., Salo H., Knappen J. H., 2010, ApJ, 721, 259
Carlberg R. G., Couchman H. M. P., 1989, ApJ, 340, 47
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Figure 13. Upper left panel shows the distance between the centres of the satellite (dE0) and the primary galaxy (gSa) as a function of time for two minor merger models (one direct and one retrograde) where merging process is delayed. Bottom left panel shows the corresponding temporal evolution of the bar strength ($S_{bar}$). Right panels shows the zoom-in view of face-on density distribution in the central 20 kpc × 20 kpc region for the host plus satellite (gSa+dE0) system, at different epochs for these models. Black lines denote the contours of constant surface density. For delayed mergers, bars survive for longer time-scales.

Chilingarian I. V., Di Matteo P., Combes F., Melchior A. L., Semelin B., 2010, A&A, 518, A61

Clamper B. C., 2016, Publ. Astron. Soc. Australia, 33, e062

Combes F., 2008, arXiv e-prints, p. arXiv:0811.0153

Coursault N., Lehner M. D., Boulanger F., Guillard P., 2018, A&A, 610, A75

Debattista V. P., Sellwood J. A., 2000, ApJ, 543, 704

Debattista V. P., Mayer L., Carollo C. M., Moore B., Wadsley J., Quinn T., 2006, ApJ, 645, 209

Dekel A., Birnboim Y., 2006, MNRAS, 368, 2

Dubinski J., Berentzen I., Shlosman I., 2009, ApJ, 697, 293

Elia-Moral M. C., González-García A. C., Balcells M., Aguerri J. A. L., Gallego J., Zamorano J., Prieto M., 2011, A&A, 533, A104

Elmegreen B. G., Elmegreen D. M., Chromey F. R., Hasselbacher D. A., Bissell B. A., 1996, AJ, 111, 2233

Elmegreen B. G., Elmegreen D. M., Hirst A. C., 2004, ApJ, 612, 191

Erwin P., Beckman J. E., Pohlen M., 2005, ApJ, 626, L81

Eskridge P. B., et al., 2000, AJ, 119, 536

Fakhouri O., Ma C.-P., 2008, MNRAS, 386, 577

Fall S. M., Efstathiou G., 1980, MNRAS, 193, 189

Feldmann R., Mayer L., Carollo C. M., 2008, ApJ, 684, 1062

Font A. S., Navarro J. F., Stadel J., Quinn T., 2001, ApJ, 563, L1

Frenk C. S., White S. D. M., Davis M., Efstathiou G., 1988, ApJ, 327, 507

Gao L., White S. D. M., Jenkins A., Stoehr F., Springel V., 2004, MNRAS, 355, 819

Gerin M., Combes F., Athanassoula E., 1999, A&A, 320, 37

Giuricin G., Mardirossian F., Mezzetti M., Monaco P., 1993, ApJ, 407, 22

Hernquist L., Weinberg M. D., 1992, ApJ, 400, 80

Hopkins P. F., Cox T. J., Younger J. D., Hernquist L., 2009, ApJ, 691, 1168

Hozumi S., Hernquist L., 2005, PASJ, 57, 719

Ibata R. A., Gilmore G., Irwin M. J., 1994, Nature, 370, 194

Ibata R., Irwin M., Lewis G., Ferguson A. M. N., Tanvir N., 2001, Nature, 412, 49

Ibata R., Chapman S., Ferguson A. M. N., Lewis G., Irwin M., Tanvir N., 2005, ApJ, 634, 287

Jogee S., et al., 2000, ApJ, 607, 1971

Kaviraj S., 2014, MNRAS, 440, 2944

Kaviraj S., Peirani S., Khochfar S., Silk J., Kay S., 2009, MNRAS, 394, 1713

Kazantzidis S., Bullock J. S., Zentner A. R., Kravtsov A. V., Mostakalas L. A., 2008, ApJ, 688, 254

Kazantzidis S., Zentner A. R., Kravtsov A. V., Bullock J. S., Debattista V. P., 2009, ApJ, 700, 1896

Kereš D., Katz N., Weinberg D. H., Davé R., 2005, MNRAS, 363, 2

Kazantzidis S., Bullock J. S., Zentner A. R., Kravtsov A. V., Mostakalas L. A., 2008, ApJ, 688, 254

Kazantzidis S., Zentner A. R., Kravtsov A. V., Bullock J. S., Debattista V. P., 2009, ApJ, 700, 1896

Keres D., Katz N., Weinberg D. H., Davé R., 2005, MNRAS, 363, 2

Lacey C., Cole S., 1993, MNRAS, 262, 627

Lang M., Holley-Bockelmann K., Sinha M., 2014, ApJ, 790, L33

Lin Y., Cervantes Sodi B., Li C., Wang L., Wang E., 2014, ApJ, 796, 98

Lokas E. L., Athanassoula E., Debattista V. P., Valluri M., Pino A. d., Semczuk M., Gajda G., Kowalczyk K., 2014, MNRAS,
Here, we show how the internal specific AM is getting distributed within different components (disc, bulge, and DM halo) of the host galaxy in a minor merger scenario. At any time $t$, the specific internal AM of the disc component is calculated using $l_{\text{int},d}(t) = \langle \mathbf{r}_d(t) \times \mathbf{v}_d(t) \rangle$, where the summation runs over all disc particles of the host galaxy. The specific internal AM for the bulge and the DM halo components are calculated in a similar fashion. The resulting temporal change in specific internal AM for different components is shown in Fig. A1.

The disc component loses specific AM, regardless of the orbital energy and orientation of the orbital spin vector. However, the initially non-rotating spherical components, namely, bulge and the DM halo, absorbs part of the orbital AM. While this broad trend holds for all minor merger models shown here, the actual amount of specific AM gain for the bulge and the DM halo components depend on the on the orbital configuration. To illustrate, the bulge and the DM halo gains more specific AM for a direct orbit when compared with a retrograde orbit with same orbital energy (compare top and bottom panels in Fig. A1). This trend is in accordance with the findings of Qu et al. (2010). The loss of specific internal AM of the disc component is seen to be accompanied by a disc heating phenomenon, causing an increase in the $v/\sigma$ parameter. For the sake of brevity, this is not shown here (for details see Qu et al. 2010).
Figure A1. Temporal change in internal specific AM shown for different components (disc, bulge, and DM halo) of the host galaxy. Top panels show for direct orbits whereas bottom panels show for the retrograde orbits. The averaging is done by the initial disc internal specific AM. Vertical arrows (in magenta) indicate the epochs of first and second pericentre passages and the epoch of merger, respectively. The individual merger models are indicated in each sub-panel.