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An Angle-Compensating, Complex-Coefficient PI Controller Used for Decoupling Control of a Permanent-Magnet Synchronous Motor

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Abstract: An asymmetric, cross-coupling effect, as well as digital control delays, in a permanent-magnet synchronous motor (PMSM) will deteriorate its current-control performance in the high-speed range, especially for electric motors used in electric vehicles (EVs) with features such as high-power density and a low carrier/modulation frequency ratio. In this paper, an angle-compensating, complex-coefficient, proportional-integrator (ACCC-PI) controller is proposed, which aims to provide an excellent decoupling performance even with considerable digital control delay. Firstly, the current open and closed loop complex-coefficient transfer functions were established in the synchronous rotation coordinate system. The proposed method, along with existing ones, were then evaluated and theoretically compared. On this basis, the parameter-tuning method of the ACCC-PI controller was presented. Finally, simulation and experimental results proved the correctness of the theoretical analysis and the proposed method.

Keywords: asymmetric cross coupling; current-loop control; digital control delay

1. Introduction

A permanent-magnet synchronous motor (PMSM) has the advantages of a compact structure, good performance, high efficiency and power density and a wide speed range. It has received a lot of attention in the field of electric vehicles (EVs) [1–5].

In a typical double-loop, control-structure based, field-oriented control (FOC) strategy of a PMSM used as drive motor, the outer loop (speed loop) determines the speed response and the inner loop (current loop) decides the steady and dynamic performance of the whole drive system. Expressed in the synchronous reference frame (dq-frame), the current control loop model is essentially a double-input, double-output (DIDO) system, and asymmetric cross coupling exists between the system of the two orthogonal dq-axes, which causes interaction of the currents of the dq-axes and induces a slow-current dynamic response [6–9]. In a typical double-loop control structure, the current loop is usually modeled as a symmetric, decoupled dq-axis, first-order system [10–12]. Thus, the DIDO system can be seen as two independent single-input, single-output (SISO) systems. However, the decoupled model is not accurate in the case of low carrier ratio. The asymmetric cross coupling is even worse due to the limited current control bandwidth and digital control delay. Normally, in the low-speed operation, the asymmetric coupling is not so significant, and its effect can be regulated without special consideration. However, in the high-speed operation, the asymmetric coupling effect between the d-axis and q-axis current dynamics becomes so significant that, without proper compensation, the current-control performance leads to instability as the fundamental frequency of the PMSM increases.
The current control plays a very important role in the PMSM control system. In order to obtain a fast, dynamic response and precise, steady-state control, many methods have been studied, e.g., predictive current control, PI control and hysteresis control [13,14]. State feedback is the most commonly used decoupling method. However, there exists a great dependence on the accuracy of the motor parameters. In [15], an improved current-decoupling controller was designed, and parameters were detected online based on the model reference-adaptive method. Feed-forward and closed-loop feedback were added to the detection system to ensure the accuracy and robustness of parameter detection, but the influence of digital control delay on the current loop was not considered. In [16], a dynamic decoupling control algorithm, using fuzzy controllers (FCs) and a neural network identifier (NNI), was proposed. Zhou compared the expressions and settings of real-coefficient and complex-coefficient PI controllers. Based on the experimental results, the advantages and disadvantages of the two PI regulators were compared in terms of decoupling of the control structure, the dynamic response speed of the current loop and parameter robustness [17]. The work of [18–20] analyzed the influence of digital control delay on system stability, and adopted the methods of double update and double sampling, along with deadbeat control to compensate it.

In this paper, current-loop control was analyzed along with complex-coefficient transfer functions, which could fully characterize the asymmetric cross coupling of the current loop and convert a DIDO system into a SISO form. Moreover, some useful methods used to analyze SISO systems, such as root locus, can be used to analyze the influence of the impedance coupling term of a PMSM and the delay angle on the stability of the current-control loop. Then, an alternative decoupling method based on a complex-coefficient, proportional-integrator (CC-PI) controller was proposed, which could prevent the current loop from being unstable in the case of low carrier ratio. On this basis, the parameter tuning method of an ACCC-PI controller was presented.

The rest of the paper is organized as follows. Section 2 presents the current open- and closed-loop, complex-coefficient transfer functions. Section 3 analyses two traditional decoupling methods and presents the proposed method. Section 4 provides the simulation and experimental results. Section 5 discusses the results of Section 4. Finally, Section 6 concludes the work and presents future work.

2. Current-Loop Modeling

2.1. Modeling of a PMSM

The typical model of a PMSM in a synchronous rotating frame is illustrated in Figure 1a. The voltage equations of a PMSM based on the extended EMF $E_{ex}$ can be expressed in matrix form, as designated in Equation (1) [21,22].

$$
\begin{bmatrix}
    u_d \\
    u_q
\end{bmatrix} =
\begin{bmatrix}
    R_s + L_d s & -\omega_r L_q \\
    \omega_r L_q & R_s + L_q s
\end{bmatrix} \times 
\begin{bmatrix}
    i_d \\
    i_q
\end{bmatrix} + 
\begin{bmatrix}
    0 \\
    E_{ex}
\end{bmatrix}
$$

(1)

where,

$$
E_{ex} = (L_d - L_q)(\omega_r i_d - s i_q) + \omega_r \cdot \psi_f
$$

(2)

$R_s$ represents the stator resistance; $\psi_f$ represents the permanent-magnet flux linkage; $\omega_r$ represents the synchronous angular velocity; $u_d$ and $u_q$ represent the $d$- and $q$-axis voltage; $i_d$ and $i_q$ represent the $d$- and $q$-axis current; $L_d$ and $L_q$ represent the $d$- and $q$-axis inductance of the PMSM, respectively.

Equation (3) can be calculated from Equation (1).

$$
\begin{bmatrix}
    i_d \\
    i_q
\end{bmatrix} =
\begin{bmatrix}
    Z_{dd}^{-1} & Z_{dq}^{-1} \\
    Z_{qd}^{-1} & Z_{qq}^{-1}
\end{bmatrix} \times 
\begin{bmatrix}
    u_d \\
    u_q
\end{bmatrix}
$$

(3)
where,

\[

dd Z^{-1} = (L_{qs} + R_s) / R \\

\quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad 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2.3. Complex-Coefficient Transfer Functions of the Current Loop

In the case of the same PI parameters, the current-loop-control model expressed by the complex-coefficient transfer functions is shown in Figure 4, where $Z = R_s + L_s j \omega_e L; \quad u_{dq} = u_d + j u_q; \quad u_{dq}' = u_{dq} + j u_{dq}' i_{dq} = i_d + j i_q; \quad i_{dq}' = i_d + j i_q'; \quad G_{PI}(s) = k_p(1 + k_i/s)$ and $j$ represents the complex sign.
3. Proposed Angle-Compensating, Complex-Coefficient PI Controller

3.1. Traditional Decoupling Method

The current feedback (CFB) [17] and complex-coefficient PI (CC-PI) [19] are the most commonly applied decoupling methods. Figure 5 shows the block diagram of the two decoupling methods.

In general, \( \omega_n << 1/T_d \) and the current open- and closed-loop, complex-coefficient transfer functions can be simplified as designated in Equations (8) and (9).

\[
G_o(s) = \frac{\omega_b (s + \omega_n)e^{-j\theta_d}}{s(s + \omega_n + j\omega_c)(T_d s + 1)} \approx \omega_b \frac{(s + \omega_n)e^{-j\theta_d}}{s(s + \omega_n + j\omega_c)} \quad (8)
\]

\[
G_c(s) = \frac{G_o(s)}{1 + G_o(s)} \approx \omega_b \frac{(s + \omega_n)e^{-j\theta_d}}{s^2 + (\omega_b e^{-j\theta_d} + \omega_n + j\omega_c)s + \omega_b \omega_n e^{-j\theta_d}} \quad (9)
\]

According to Figure 5, the current closed-loop, complex-coefficient transfer functions, with a decoupling method, can be deduced as designated in Equations (10) and (11).

\[
G_{c,CFB}(s) = \frac{\omega_b (s + \omega_n)e^{-j\theta_d}}{s(s + \omega_n + j\omega_c e^{-j\theta_d}) + \omega_b (s + \omega_n)e^{-j\theta_d}} \quad (10)
\]

\[
G_{c,CCPI}(s) = \frac{\omega_b e^{-j\theta_d}}{s + \omega_b e^{-j\theta_d}} \quad (11)
\]

By comparing Equations (10) and (11), both decoupling methods could decouple the current loop as a first-order inertial link with \( \theta_d = 0 \) rad. However, the CC-PI decoupling method had a simpler closed-loop transfer expression when a digital delay was added. The closed-loop poles can be expressed using Equation (12).

\[
s = -\omega_b \cdot \cos(\theta_d) + j\omega_b \cdot \sin(\theta_d) \quad (12)
\]

The pole in the right half plane appeared only when the delay angle \( \theta_d > \pi/2 \) rad, which meant the current loop became unstable.

On the contrary, the closed-loop pole expression of the CFB decoupling method was very complicated and more parameter-sensitive. The performance of the two decoupling methods with angle delay was compared through simulation in Section 4.1.
3.2. Proposed ACCC-PI Controller

The structure of the proposed ACCC-PI decoupling current controller is shown in the shadow box outlined with a dotted line in Figure 6, which had the mixed structure of direct PI controllers, the cross-coupling integral controllers and the angle-compensating part.

The complex-coefficient transfer function of the ACCC-PI controller was obtained as designated in Equation (13).

\[ G_{ACCC-PI}(s) = G_r(s) + jG_i(s) \]  

(13)

\[ \begin{align*}
G_{rd}(s) &= k_{pd} \cos \hat{\theta}_d + k_{pd} k_{id} \cos \hat{\theta}_d - k_{pd} k_{id} \sin \hat{\theta}_d \\
G_{iq}(s) &= k_{pq} \sin \hat{\theta}_d + k_{pq} k_{iq} \sin \hat{\theta}_d - k_{pq} k_{iq} \cos \hat{\theta}_d \\
G_{q}(s) &= k_{pq} \cos \hat{\theta}_d + k_{pq} k_{id} \cos \hat{\theta}_d - k_{pq} k_{id} \sin \hat{\theta}_d \\
G_{i}(s) &= k_{pq} \sin \hat{\theta}_d + k_{pq} k_{id} \sin \hat{\theta}_d - k_{pq} k_{id} \cos \hat{\theta}_d
\end{align*} \]  

(14)

Figure 6. Block diagram of current-loop control with the ACCC-PI controller.

Figure 7 shows the current-loop control block diagram with the proposed ACCC-PI controller. Symbol “ˆ” represents the estimated value. Where,

\[ \begin{align*}
G_{rd}(s) &= k_{pd} \cos \hat{\theta}_d + k_{pd} k_{id} \cos \hat{\theta}_d - k_{pd} k_{id} \sin \hat{\theta}_d \\
G_{iq}(s) &= k_{pq} \sin \hat{\theta}_d + k_{pq} k_{iq} \sin \hat{\theta}_d - k_{pq} k_{iq} \cos \hat{\theta}_d \\
G_{q}(s) &= k_{pq} \cos \hat{\theta}_d + k_{pq} k_{id} \cos \hat{\theta}_d - k_{pq} k_{id} \sin \hat{\theta}_d \\
G_{i}(s) &= k_{pq} \sin \hat{\theta}_d + k_{pq} k_{id} \sin \hat{\theta}_d - k_{pq} k_{id} \cos \hat{\theta}_d
\end{align*} \]  

Model of PMSM

Figure 7. Current-loop control block diagram with the ACCC-PI controller.

If \( \hat{\theta}_d = \theta_d, \hat{\psi}_i = \psi_i \), the control block diagram of the current loop of the permanent-magnet synchronous motor is illustrated in Figures 8 and 9.
If \( L_d = L_q; L_q = L_{iq}; R_s = R_{iq} \), after the adoption of the proposed ACCC-PI controller, the current closed-loop complex-coefficient transfer function is illustrated in Equation (15).

\[
G_{c_{ACCCPI}}(S) = \omega_b / (s + \omega_b)
\]  

(15)

According to Equation (15), the current loop had a negative, real-part closed pole \((-\omega_b, 0\)), and the performance of the current loop was only related to the control bandwidth.

4. Simulations and Experiments

The simulations and experiments were built according to the parameters of the PMSM in Table 1. Figure 10 shows the control block diagram used in the experiment. The control algorithm was realized through a 32-bit processor TMS320F28335, and the inverter stack was made of a drive module designed for hybrid- and electric vehicle applications (PS820R08A6P2B). We used the PMSM with parameters listed in Table 1 and set the experimental conditions to be the same as those of the simulation. Figures 11 and 12 shows the experiment platform.
The simulations and experiments were built according to the parameters of the PMSM. Table 1.

| Parameters                          | Value     |
|-------------------------------------|-----------|
| Pole pairs                          | 6         |
| Phase resistance                    | 8 [mΩ]    |
| d-axis inductance                   | 0.16 [mH] |
| q-axis inductance                   | 0.16 [mH] |
| Permanent-magnet flux linkage       | 0.0488 [Wb] |

![Control block diagram used in the experiment.](image1)

Figure 10. Control block diagram used in the experiment.

![Block diagram of the experiment.](image2)

Figure 11. Block diagram of the experiment.
Figure 12. Back-to-back test platform.

4.1. Simulations of Different Decoupling Algorithms

The simulated $dq$-axes' current response without a decoupling algorithm is illustrated in Figure 13, the cross coupling of the current-control loop was aggravated and the dynamic response became negatively affected by the motor impedance coupling (MIC) and digital control angle delay (AD).

![Simulation waveform of $dq$-axes' current response](image)

Figure 13. Simulation waveform of $dq$-axes' current response affected by the motor impedance coupling (MIC) term and digital control angle delay term, the PI parameters of the current-control loop were (kp = 0.3, ki = 50) and the rotor electrical angular velocity $\omega_e$ was 1256 rad/s. (a) $d$-axis current response; (b) $q$-axis current response.

The performance of the three decoupling methods was compared through simulation in the same conditions, as shown in Figure 14.

At the beginning of the simulation, the current command of the $d$- and $q$-axis were all zero, and the $-200\text{A}$ current step command of the $q$ axis occurred at 0.8 s. The decoupling and dynamic performance of the algorithm were evaluated by observing the current response of $d$- and $q$-axis. As shown in Figure 14a, according to Equations (13) and (14), the CFB and CC-PI methods had the same decoupling effect without considering the digital control delay angle, that is, there was no fluctuation in the $d$-axis current and there was the same dynamic performance of the $q$-axis current. However, when the digital control delay angle was taken into account in Figure 14b, the CC-PI decoupling method had better dynamic response characteristics than the CFB decoupling method under the same simulation conditions, but still had a coupling current in the $d$-axis. The coupling $d$-axis current disappeared when the proposed ACCC-PI controller was used.
Figure 14. *dq*-axes’ current-response simulation waveform using different decoupling algorithms, the PI parameters of the current-control loop were (kp = 0.3, ki = 50), rotor electrical angular velocity \( \omega_e \) was 1256 rad/s. (a) *dq*-current response using the CFB and CCPI decoupling methods, regardless of the angle delay; (b) *d*-axis current response with angle delay; (c) *q*-axis current response with angle delay.

4.2. Experiments of Different Decoupling Algorithms

The proposed method of ACCC-PI was experimentally verified by the back-to-back test platform as shown in Figure 12. The performance of the three decoupling methods was compared through simulation in the same conditions, as shown in Figure 14. The PI parameters of the current-control loop were (kp = 0.3, ki = 50), rotor electrical angular velocity \( \omega_e \) was 1256 rad/s and the motor speed was 2000 rpm.
Figure 15. Cont.
Figure 15. Comparison of current response using different algorithms under the q-axis current-command step. (a) Phase current waveform; (b) d-axis current response; (c) q-axis current response.

The experimental results were basically consistent with the theoretical and simulation results, the proposed ACCC-PI controller had the best dynamic performance and decoupling effects. As shown in Figure 15b,c, when the −200A step occurred in the q-axis current command, the CC-PI decoupling method had better q-axis current dynamic response than the CFB decoupling method (same as the simulation results in Figure 14c), but still had a coupling current in the d-axis (about −100A). However, the proposed ACCC-PI decoupling method had the smallest coupling d-axis current (−25A) and the best q-axis current dynamic performance (with non-overshoot and fast response).

5. Discussion

In order to reduce the weight and volume of the PMSM drive system, the speed of the PMSM was high and the polar number was large. Limited by the efficiency requirements of the controller and the heat dissipation of power devices, the control switch frequency was small. It can be seen from the simulation that, in the case of low carrier ratio, the motor’s own impedance coupling led to a deterioration in current-loop performance. After the addition of angle delay, the coupling effect became more serious, the overshot of the q-axis current was larger and the response was slower, and the amplitude of the d-axis coupling current was larger.
Compared with the traditional two decoupling methods, when the angle delay was not considered, it could be seen from the complex-coefficient transfer functions that both methods could decouple the current loop to the first-order system. Therefore, there was no fluctuation of $d$-axis current and the same dynamic performance of $q$-axis current could be seen. However, after the angle delay was added, the complex-coefficient transfer function of the CC-PI decoupling method was simpler. The pole in the right half plane appeared only when the delay angle $\theta_d > \pi/2$ rad, which meant that the current loop became unstable. On the contrary, the closed-loop pole expression of the CFB decoupling method was very complicated and more parameter-sensitive. Simulation and experimental results showed that the CC-PI decoupling method had better dynamic response characteristics than the CFB decoupling method.

After adopting the proposed ACCC-PI controller, the current loop had a negative real-part closed pole $(\omega_b, 0)$, and the performance of the current loop was only related to the control bandwidth. Compared with the CC-PI and CFB decoupling method, the proposed ACCC-PI decoupling method had the smallest coupling $d$-axis current and the best $q$-axis current dynamic performance. However, due to the change of motor inductance and other parameters, the perfect decoupling effect achieved in simulation could not be realized in the experiment.

6. Conclusions

The model of the PMSM and the angle delay model of the digital system, which had similar coupling structures, were established in this paper. The traditional decoupling method only compensated for the impedance coupling term of the PMSM, and did not consider the coupling effect caused by the delay angle. Based on the derivation and analysis of the complex-coefficient transfer functions of the current loop, an angle-compensating, complex-coefficient PI (ACCC-PI) controller was proposed. Using the ACCC-PI controller proposed in this paper, the $q$-axis current response was fast and there was no overshoot. The performance was basically the same as that of the CC-PI decoupling method, and the coupling $d$-axis current amplitude was the minimum. However, due to the changes of motor resistance, inductance and other parameters in the actual system, the $d$-axis coupling current in the experiment was not completely eliminated, and further optimization research on the influence of motor parameters on decoupling performance is still needed.

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