A non-LTE spectral analysis of the $^3$He and $^4$He isotopes in the HgMn star $\kappa$ Cancri*,**

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ABSTRACT

Aims. We present a pilot study on non-local thermodynamic equilibrium (NLTE) line-formation computations for the isotopes $^3$He and $^4$He in the mercury-manganese star $\kappa$ Cancri. The impact of NLTE effects on the determination of isotopic abundances and the vertical stratification of helium in the atmosphere is investigated.

Methods. Modern NLTE line-formation computations were employed to analyse a high-resolution and high-signal-to-noise ratio ESO-VLT/UVES spectrum of $\kappa$ Cnc. The atmospheric parameters were determined from fitting the hydrogen Balmer lines and the spectral energy distribution. Multiple He I lines were investigated, including He I 4921 Å and 6678 Å, which show the widest isotopic splits.

Results. Half of the observed He I lines in the spectrum of $\kappa$ Cnc show significant NLTE strengthening, the effects are strongest in the red lines He I 4587 Å and He I 4667 Å. NLTE abundances from individual He I lines are up to a factor of ~3 lower than LTE values. Helium is found to be stratified in the atmosphere of $\kappa$ Cnc. While the LTE analysis indicates a step-like profile of the helium abundance, a gradual decrease with height is indicated by the NLTE analysis. A $^4$He/$^3$He ratio of ~0.25–0.30 is found. With the available data it cannot be decided whether the two isotopes follow the same stratification profile, or not.

Conclusions. This work implies that NLTE effects may be ubiquitous in the atmospheres of HgMn stars and may have a significant impact on abundance determinations and the interpretation of the vertical abundance stratification of elements.

Key words. stars: abundances – stars: atmospheres – stars: chemically peculiar – stars: early-type – stars: individual: $\kappa$ Cancri

1. Introduction

Mercury-manganese stars are chemically peculiar (CP) stars of the upper main sequence, with the line spectra of Hg II and Mn II indicating large overabundances of the two elements. They constitute Preston’s subgroup CP3 (Preston 1974). Their effective temperatures range between 10,500 and 16,000 K, corresponding to spectral types A0 to B6 (Smith 1996). Some other distinctive characteristics of these stars are low rotational velocities ($v \sin i \leq 29$ km s$^{-1}$, Abt et al. 1972) and overabundances of other elements such as P, Ga, Y, and Pt, with abundance patterns changing from one star to the other. They can show an inhomogeneous distribution of some chemical elements over their surface (first discussed by Hubrig & Mathys 1995), which causes the observed line-profile variability in the spectra (e.g. Hubrig et al. 2011). HgMn stars are members of binaries in more than 50% of the cases, with periods ranging between 3 to 20 days (Gerbaldi et al. 1985).

The chemical peculiarities in the atmospheres of HgMn stars arise because of their extremely stable atmospheres, exposing the atoms and ions to the competitive actions of gravitational settling and radiative levitation. The observed abundance peculiarities can in principle be explained within the framework of atomic diffusion (Michaud et al. 1979). Diffusion theory predicts that the photospheres of all HgMn stars should be deficient in helium, which was confirmed for instance in a dedicated study by Dworetsky (2004). The reason is that helium has only few and weak lines at wavelengths where the stellar flux is high (longward of the Lyman edge), therefore gravitational settling dominates. Dworetsky also found evidence for a vertical helium abundance stratification in two HgMn stars, which would also be a consequence of atomic diffusion in the atmosphere.

Moreover, helium is a particular case for the occurrence of differential effects of diffusion on the isotopes of an element. The mass difference between its two isotopes, $^3$He and $^4$He, is largest among the light elements, with gravitational settling favouring the heavier isotope. Some CP stars can therefore show enhanced $^3$He well above the protosolar $^3$He/$^4$He ratio of $(1.66 \pm 0.05) \times 10^{-4}$ (Mahaffy et al. 1998). This is most * Based on data products from observations made with ESO Telescopes at the La Silla Paranal Observatory under programme ID 076.B-0055(A).
** Figures 3 and 4 are available in electronic form at http://www.aanda.org
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pronounced for the (He-weak) $^3$He stars, which occupy a narrow strip in the log $T_{\text{eff}}$–log $g$ plane between the He-strong B stars and a group of He-weak B stars that show no evidence of $^3$He. However, the presence of a significant amount of $^3$He was also suggested for some HgMn stars (Hartoog & Cowley 1979).

Analyses of helium abundances in CP stars (and also for other elements) have so far mostly been performed under the assumption of local thermodynamic equilibrium (LTE). On one hand, this was possibly motivated by the early non-LTE (NLTE) study by Auer & Mihalas (1973), who found that the blue-violet He I lines are described well under the assumption of LTE in the temperature range below 15,000 K. On the other hand, this has also practical reasons because LTE line-formation can be much easier implemented than NLTE modelling. However, the quality of the observations has improved tremendously over the past decades, and we consider the topic worth to merit a re-visit in an era where quantitative spectroscopy can be performed at high precision and accuracy. A more consistent NLTE modelling of CP stars may therefore help in developing a quantitatively refined view of defusion theory, which is required to explain the variety of observed abundance peculiarities even within one class of CP stars.

We chose the prototype HgMn star $\kappa$ Cancri (HD 78316, HR 3623) for a pilot study that aims at re-investigating the topic based on our latest NLTE models. This well-known sharp-lined star was reported to be a possible $^3$He star by Hartoog & Cowley (1979), who derived an upper limit on the $^3$He/$^4$He ratio of 0.35, more than a thousand times higher than the protosolar value. The presence of $^3$He in the photosphere of this star was confirmed by Dobričev et al. (1989) and Zakharova & Ryabchikova (1996), concluding on a value of the $^3$He/$^4$He ratio of 0.35. These previous works were all based on LTE modelling and spectra at lower resolution than available today. Here, we investigate NLTE effects and their impact on the determination of (isotopic) abundances and the vertical stratification of helium, considering various He I lines.

2. Observational data

The spectrum employed in the present work was observed with UVES (UV-Visual Echelle Spectrograph, Dekker et al. 2000) on the ESO VLT/UT2 at Cerro Paranal in Chile under the program 076.B-0055(A). We extracted the pipeline-reduced spectrum from the ESO Science Archive Facility. The spectrum was obtained in dichroic mode, covering the spectral range $\lambda\lambda$ 3700–10,200 Å (with a small gap in the region of the near-IR calcium triplet), at resolving power $R = \lambda/\Delta\lambda \approx 110,000$. The peak signal-to-noise ratio is $\sim$270. To normalize of the spectrum we fitted a spline function to a number of continuum windows.

In addition, (spectro-)photometric data were adopted from the literature to construct the spectral energy distribution (SED) of $\kappa$ Cnc. $UBV$ photometry was adopted from Mermilliod (1991) and $JHK$ data from the Two Micron All Sky Survey (2MASS, Skrutskie et al. 2006). Two low-dispersion spectra that were observed with the International Ultraviolet Explorer (IUE) using a large aperture were extracted from the MAST archive. The exposures SWP06911 and LWR05873 cover the range from 1150 to 1980 Å and from 1850 to 3290 Å.

3. Model calculations

We employed a hybrid NLTE approach for our line-formation calculations, which has been successfully used before for quantitative analyses of main-sequence OB stars (Nieva & Przybilla 2007, 2008), their evolved progeny (Przybilla et al. 2006a), and subdwarf B stars (Przybilla et al. 2006b). Model atmospheres were computed with the code ATLAS9 (Kurucz 1993), which assumes plane-parallel geometry, chemical homogeneity, and hydrostatic, radiative, and LTE. A value of triple solar metallicity was adopted for the model atmosphere calculations for $\kappa$ Cnc, which is found to reproduce the low-resolution UV spectrum overall well.

Then, NLTE line-formation computations were performed with the codes DETAIL and SURFACE (Giddings 1981; Butler & Giddings 1985). DETAIL calculates atomic-level populations by solving the coupled radiative transfer and statistical equilibrium equations, and SURFACE computes the formal solution using realistic line-broadening functions. The following model atoms were employed: H (Przybilla & Butler 2004), He I (Przybilla 2005), and, for some supplementary calculations, O I/II (Przybilla et al. 2000; Becker & Butler 1988, updated). To facilitate NLTE calculations for the $^3$He isotope in addition to the usual $^4$He, a $^3$He model atom in analogy to that of $^4$He by Przybilla (2005) was realized, taking into account isotopic line shifts as measured by Fred et al. (1951). Both isotopes were treated simultaneously to account for the overlap of lines and continua.

Our approach allows LTE spectrum synthesis to be performed by running SURFACE only on top of the ATLAS9 model. In this case, LTE level populations are computed while all other model ingredients remain unchanged, which facilitates assessing the impact of NLTE effects.

4. Atmospheric parameter determination

$\kappa$ Cnc is a known single-lined spectroscopic binary (SB1) star. The system has been resolved among others by Schöllner et al. (2010), who found a $\sim$2.5 mag difference in the $K$ band between the primary and the (later-type) secondary. Because the brightness ratio increases towards shorter wavelengths, we do not expect the available spectrum to be contaminated by any significant second light.

Therefore, the analysis of the observed spectrum followed a similar philosophy as previously employed by us for studies of normal B-type stars in Nieva & Przybilla (2007, 2012). We used the hydrogen Balmer lines and the SED as principal indicators to determine the effective temperature $T_{\text{eff}}$ and the surface gravity log $g$. Supplementary indicators were two hydrogen Paschen lines and the ionization balance of O I/II. A fine-tuning of the atmospheric parameters was achieved by multiple iterations aiming at reproducing all indicators simultaneously. At this stage of the analysis, an approximate average value for the helium abundance in the line-formation region was determined, which had to be assumed to be homogeneous throughout the entire atmosphere because of the basic assumptions made in ATLAS9. Note that this introduces no restrictions to the further discussion, as helium behaves as a trace element in our case. A zero microturbulent velocity $\xi$ was adopted, which facilitates reproducing the

1 http://archive.stsci.edu/

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weak and strong oxygen lines for one abundance value simultaneously. The (radial-tangential) macroturbulent velocity \( \zeta \) and projected rotational velocity \( v \sin i \) were also determined based on fits to the oxygen lines. The finally adopted atmospheric parameters together with a few supplementary data are summarised in Table 1. Our \( T_{\text{eff}} \) is significantly lower (by up to \( \sim 1000 \) K in the extremes) and the \( \log g \) slightly lower than in earlier LTE analyses (e.g. Roby & Lambert 1990; Dworetsky & Budaj 2000; Adelman et al. 2004; Bailey & Landstreet 2013; Takeda et al. 2014). The higher temperatures are not compatible with the observed SED. On the other hand, our results agree excellently well with the atmospheric parameters adopted by Zakharova & Ryabchikova (1996) and Maza et al. (2011).

Figures 1 and 2 show a comparison of a global (by-eye) best-fit NLTE spectrum with \( \text{H}\beta \) to He and the fit of the ATLAS9 model flux to the observed SED. For the latter, the photometric data were converted into fluxes using zeropoints of Bessell et al. (1998) for Johnson photometry and of Heber et al. (2002) for the 2MASS photometry. All observed fluxes were de-reddened using an interstellar reddening law according to Cardelli et al. (1989), adopting a colour excess \( E(B-V) \) as indicated in Table 1 and a ratio of total-to-selective extinction \( E(B-V) = A_V/E(B-V) = 3.1 \). Overall, good agreement between model and observation is achieved. This also includes the confirmation of the atmospheric parameter determination by the secondary indicators, the Paschen lines \( \text{P}_11 \) and \( \text{P}_12 \) (the only useful lines from the near-IR region, see Fig. 3) and the \( \text{O}/\text{He} \) NLTE ionization balance (see Fig. 4). The latter is fulfilled for a homogeneous oxygen abundance of \( \log (\text{O}/\text{H}) + 12 = 8.40 \), without any indication for a depth-dependent abundance stratification of this element.

5. Helium abundance analysis

The visual inspection of the helium spectrum of \( \kappa \) Cnc shows two peculiarities. First, an asymmetry of \( \text{He}\text{i} \, \lambda 4921.9 \) Å and a resolved second component redwards of \( \text{He}\text{i} \, \lambda 6678.1 \) Å indicate the presence of the \(^3\text{He} \) isotope in the stellar atmosphere (see Fig. 5), confirming the detection of Hartoog & Cowley (1979) at much higher spectral resolution (cf. also Zakharova & Ryabchikova 1996). Second, the strongest among the diffuse \( \text{He}\text{i} \) lines, at \( \lambda 4026.2 \) Å and \( \lambda 4471.5 \) Å, show shallow cores in combination with unusually broad wings (see Fig. 6). This is a clear sign that the element is not homogeneously distributed.

Table 1. Atmospheric parameters.

| Parameter         | \( \kappa \) Cnc |
|-------------------|------------------|
| Sp. Type          | B8 III           |
| \( V \) (mag)     | 5.233            |
| \( B-V \) (mag)   | -0.113           |
| \( E(B-V) \) (mag)| 0.038            |
| \( T_{\text{eff}} \) (K) | 12 800 ± 200 |
| \( \log g \) (cgs)| 3.70 ± 0.10     |
| \( v \sin i \) (km s\(^{-1}\)) | 6 ± 2        |
| \( \zeta \) (km s\(^{-1}\)) | 4 ± 2        |

Fig. 1. Comparison of our global best-fit NLTE synthetic spectrum (red line) with observed spectral lines of \( \text{H}\beta \) to He (black line) in \( \kappa \) Cnc.

Fig. 2. Comparison of the ATLAS9 model flux (red line) for our adopted atmospheric parameters with the observed SED (black line and boxes). Values of colour excess and the ratio of total-to-selective extinction employed in the de-reddening of the observations are indicated.

Fig. 5. Comparison of our NLTE spectrum synthesis (red lines) with observation for the two lines with the widest isotopic separation (black lines). Synthetic LTE spectra computed for the same isotopic helium number fractions are also shown (dotted red line). The positions of the line centres of the isotopic components are indicated.
can be derived (we kept the 3He lines, such that only a combined abundance from both isotopes the value of 0.35 derived by Zakharova & Ryabchikova (1996). spheric depths covered by the observations, slightly lower than A112, page 4 of 7

dance stratification, which is unusual in HgMn stars and has throughout the atmosphere, but instead shows a vertical abundance stratification, which is unusual in HgMn stars and has been reported for only a few objects so far (Dworetsky 2004; Castelli & Hubrig 2007).

The quantitative analysis of the He I spectrum uses line-profile fits to the observed (largely) unblended features (He I λλ 4009.3 Å, 5015.7 Å, and 5047.7 Å are strongly blended with metal lines). The individual best fits from the NLTE modelling to the two lines with resolved isotopic contributions are shown in Fig. 5. For comparison, LTE profiles for the same de-

Table 2. Isotopic helium abundances.

| λ (Å)  | log τ_{Ross} | ε(He)_{NLTE} | ε(He)_{LTE} |
|------|-------------|--------------|-------------|
| 3He | 4921.9 | -0.061 | 0.0070 | 0.0087 |
| 3He | 4922.3 | 0.001 | 0.0027 | 0.0032 |
| 4He | 6678.1 | -0.362 | 0.0070 | 0.0185 |
| 3He | 6678.7 | -0.256 | 0.0018 | 0.0032 |

Table 3. Line-by-line abundances of He I.

| λ (Å)  | log τ_{Ross} | ε(He)_{NLTE} | ε(He)_{LTE} |
|------|-------------|--------------|-------------|
| 3867.5 | 0.179 | 0.020 | 0.020 |
| 4026.2 core | 0.045 | 0.007 | 0.008 |
| 4026.2 wing | 0.213 | 0.017 | 0.017 |
| 4120.8 | 0.105 | 0.015 | 0.016 |
| 4387.9 | 0.098 | 0.013 | 0.015 |
| 4437.6 | 0.142 | 0.024 | 0.024 |
| 4471.5 core | -0.146 | 0.008 | 0.011 |
| 4471.5 wing | 0.167 | 0.024 | 0.024 |
| 4713.2 | -0.001 | 0.010 | 0.012 |
| 5875.6 | -0.373 | 0.004 | 0.011 |

Fig. 6. Comparison of our two-component NLTE fits with the strongest observed diffuse He I lines. The upper curves in each panel visualise the fit to the line wings, the lower ones the fit to the line core. See Fig. 5 for the description of the line encoding. The two vertical lines indicate the degree of the isotopic shift in the two cases.

Fig. 7. Comparison of our NLTE spectrum synthesis with all other He I lines that were analysed here. Shown are individual best fits. Lines are encoded in the same way as in Fig. 5.

abundances are summarised in Table 3 in analogy to Table 2. Data for the wings of the lines were evaluated 2 Å redwards of the line core. In the cores of the two lines, NLTE abundances are smaller than derived in LTE, by about 15% and 40%. The wings are unaffected by NLTE effects. Individual best fits to all other He I lines that were analysed here are shown in Fig. 7, with the results summarised in Table 3. Typically, NLTE effects are weak in these mostly weak lines. Strong effects are present only in He I λ5875.6 Å, implying that the NLTE abundances are lower than the LTE values by a factor of almost 3.

NLTE effects. Departure coefficients b_j = n_j/n_j^* (Zwaan definition, the n_j and n_j^* are the NLTE and LTE level population numbers) for the helium energy levels are displayed in Fig. 8 as a function of optical depth. He I is the main ion at the temperatures found in the visible layers of the atmosphere of κ Cnc. The population of the He I ground state shows practically no deviations from detailed equilibrium. The levels with principal quantum number n = 2 are overpopulated relative to LTE values (the 2s1S levels are not shown in Fig. 8 for clarity, as they show qualitatively and quantitatively a very similar behaviour as the 2p1P levels). This is because radiative (the 2s 1S state is metastable) and collisionally induced decays to the ground state are inefficient, while the level populations are constantly fed by the recombination cascade from higher levels, which drains the
populations of these. In consequence, all higher levels are underpopulated compared with the LTE values. They closely follow the behaviour of the He\(\text{II}\) ground state. Detailed balance is approached for all levels at continuum formation depths (at \(\log \tau_{\text{Ross}} \approx 0.2 - 0.3\)) and below, the NLTE population numbers differ at most by a few percent from LTE values in the line-formation region (see Tables 2 and 3). The differences in the behaviour of the departure coefficients between \(^3\)He and \(^4\)He levels are negligible. All the He\(\text{I}\) lines that were analysed here have either the 2p\(^1\)P\(_0\) or the 2p\(^3\)P\(_0\) level as the lower transition level and upper levels with a higher principal quantum number. Therefore, NLTE strengthening of the lines can occur as the consequence of overpopulated lower and underpopulated upper levels, depending on the formation depth. The (stronger) red He\(\text{I}\) lines are more sensitive to NLTE effects also because of the pronounced differential effects of the line-source function to variations of the departure coefficients in the Rayleigh-jeans limit (see e.g. Przybilla & Butler 2004). Even small differences in level populations on the percent-level can therefore result in fundamentally altered line strengths.

6. Discussion

Using abundances from lines of different strength – which sample the line-formation region to a different extent –, one can reconstruct the abundance profile, that is, the vertical abundance stratification of an element in the atmosphere. The run of the helium number fraction \(\epsilon(\text{He})\) with optical depth in the atmosphere of \(\kappa\) Cnc is shown in Fig. 9. The LTE analysis indicates a step-like helium stratification, dropping in the region \(\log \tau_{\text{Ross}} \approx 0.2\) to 0.1 from a high abundance of \(\epsilon(\text{He}) = 0.25\) to a constant value of about half of that farther outward in the atmosphere. On the other hand, the stratification derived from the NLTE analysis implies a gradual decrease of the helium abundance with decreasing optical depth, which is a qualitatively different behaviour. The NLTE abundances are lower by almost a factor 3 at the lowest optical depths that can be traced. Note that while the formation regions of the weaker lines agree well when computed under LTE and NLTE conditions, they can differ by up to \(\sim 0.1\) dex in \(\log \tau_{\text{Ross}}\) for the stronger lines. The LTE computations indicate a formation of the line cores farther out in the atmosphere.

It would be highly interesting to know whether the two helium isotopes follow the same stratification profile, or if differential effects prevail. Unfortunately, with data from only two lines this cannot be decided here with confidence.

Finally, it may be appropriate here to comment on NLTE effects in CP stars in the general context, based on the present findings. The helium lines in \(\kappa\) Cnc are weak because of the rather low \(T_{\text{eff}}\) for populating the excited levels and because of the low helium abundance that is due to gravitational settling. Nevertheless, NLTE effects are found for all but the weakest He\(\text{I}\) lines, leading to changes in the derived abundances relative to an LTE analysis by up to a factor \(\sim 3\). On the other hand, most of the metals show large overabundances because of radiative levitation, yielding spectral lines much stronger than usually found in normal stars. The formation regions for the strong lines extend to much lower optical depths than investigated here, possibly giving rise to much stronger NLTE effects than encountered in the present work. More NLTE studies for CP stars are encouraged because this may have a significant effect on the results of elemental abundance determinations and on the deduced abundance stratifications.

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References

Abt, H. A., Chaffee, F. H., & Suffolk, G. 1972, ApJ, 175, 779
Adelman, S. J., Proffitt, C. R., Wahlgren, G. M., Leckrone, D. S., & Dolk, L. 2004, ApJS, 155, 179
Auer, L. H., & Mihalas, D. 1973, ApJS, 25, 433
Bailey, J. D., & Landstreet, J. D. 2013, A&A, 551, A30
Becker, S. R., & Butler, K. 1988, A&AS, 74, 211
Bessell, M. S., Castelli, F., & Plez, B. 1998, A&A, 337, 321
Butler, W. P., & Giddings, J. R. 1985, in Newsletter of Analysis of Astronomical Spectra, No. 9 (Univ. London)
Cardelli, J. A., Clayton, G. C., & Mathis, J. S. 1989, ApJ, 345, 245
Castelli, F., & Hubrig, S. 2007, A&A, 475, 1041
Dekker, H., D’Odorico, S., Kaufer, A., Delabre, B., & Kotzlowski, H. 2000, Proc. SPIE, 4008, 534
Dobruchev, V. M., Raikova, D. V., Ryabchikova, T. A., & Topil’skaya, G. P. 1989, Afz, 30, 91
Dworetsky, M. M. 2004, in The A-Star Puzzle, eds. J. Zverko, J. Ziznovsky, S. J. Adelman, & W. W. Weiss, IAU Symp., 224, 727
Dworetsky, M. M., & Budaj, J. 2000, MNRAS, 318, 1264

Fig. 8. Departure coefficients \(b_i\) of the \(^4\)He (full lines) and the \(^3\)He levels (dotted lines) as a function of optical depth for a model with \(\epsilon(\text{He}) = 0.008\) and \(\epsilon(\text{He}) = 0.002\). Level designations or principal quantum numbers \(n\) of the levels are indicated. The dots mark the run of the He\(\text{II}\) ground-state departure coefficient.

Fig. 9. Helium number fraction as a function of Rosseland optical depth in the atmosphere of \(\kappa\) Cnc (NLTE results: dots, LTE: circles).
Fig. 3. Comparison of our global best-fit NLTE synthetic spectrum (red line) with the observed Paschen lines Pa11 and Pa12 (black line) in κ Cnc.

Fig. 4. Comparison of our global best-fit NLTE synthetic spectrum (for log (O/H) + 12 = 8.40, red) with the observed O i/ii lines (black lines) in κ Cnc.