Calculating the variations of sunrise, sunset and day length times for Baghdad city. With comparison to different regions of the world in year 2019

Fouad M. Abdulla
Department of Astronomy and Space, College of Science, University of Baghdad, Baghdad, Iraq

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Introduction
The time of sunrise at any place is the moment when the upper edge of the Sun appears above the horizon in the morning. The time of sunset is defined as the moment when the upper edge of the sun...
Sun disappears below the horizon, while the day length period is the interval time between sunrise and sunset [1].

The sunrise, sunset, and day length times for a certain place vary from day to day during the year, and near the horizon. Atmospheric refraction causes distortion of sunlight rays to such an extent that geometrically the solar disk is already about one diameter below the horizon when a sunset was observed [2] (Figure 1).

![Figure 1-The Sun at sunrise, with the effects of atmospheric refraction [3].](image)

Light is refracted through the atmosphere on its way to the earth’s surface. This causes the sun to appear higher in the sky than it really is (Figure 1). Sunrise occurs before the Sun actually reaches the horizon because the sunlight is refracted by the Earth's atmosphere. At the horizon, the average amount of refraction is 34 arcminutes, although this amount varies based on atmospheric conditions [4].

In addition, sunrise occurs when the Sun's upper limb, rather than its center, appears to cross the horizon. The apparent radius of the Sun at the horizon is 16 arcminutes. These two angles combine to define sunrise to occur when the Sun's center is 50 arcminutes below the horizon, or 90.83° from the zenith [5].

1. **Date and Julian Date**

Julian Date (JD) is the number of days and fractions beginning from mean noon on January 1st, 4713 BC [6,7].

The program must then starts with a procedure to separate the numbers of years (y), months (m), d = day + U.T / 24

Where U.T: is the epoch universal time in hours.

In what follows, we will suppose that separation has been performed.

At m = 1 or 2, take (to solve February month problem)

y = y – 1 and m = m + 12.

If the number y, m, and d are equal or larger than 1582/10/15 (that is, in the Gregorian calendar), calculate as [8]:

\[ A_j = \text{INT} \left( \frac{y}{100} \right) \]

\[ B_j = 2 - A_j + \text{INT} \left( \frac{A_j}{4} \right) \]

Before the date 1582/10/15, Bj = 0

The required Julian Day is then [14]:

\[ JD = \text{INT} \left( 365.25 \times y \right) + \text{INT} \left( 30.6001 \times (m + 1) \right) + d + 1720994.5 + B_j \] (1)
$T_2$ denotes the number of Julian centuries from the epoch J2000.0. It is calculated by the following formula [9,10]:

$$T_2 = \frac{JD - 2451545.5}{36525}$$  \hspace{1cm} (2)

2. Coordinates of the Sun

2.1 Ecliptical Coordinates of the Sun

The longitude of the sun on the epoch J2000.0 was 280.46 and the rate at which the Earth is going around the Sun is 0.985647359 per day (from equinox to equinox), and the mean longitude of the Sun was applied as in previous studies [11,12]:

$$L_s = 280.46 + 36000\cdot7693T_2 + 0.003032T_2^2$$  \hspace{1cm} (3)

The longitude of perigee of Earth's orbit on the epoch J2000.0 was 357.528 and the rate at which the Sun is moving from perigee to perigee is 0.985600281 per day, while the mean anomaly was applied as previously described [13]:

$$M_s = 257.52911 + 35999\cdot05029T_2 - 0.0001537T_2^2$$  \hspace{1cm} (4)

The Sun's equation of the center $C_s$ is [14]:

$$C_s = 1.914602 - 0.004817T_2 - 0.000014T_2^2 \sin (M_s) + (0.019993 - 0.000101T_2) \sin (2M_s) + 0.000289 \sin (3M_s)$$  \hspace{1cm} (5)

The true longitude of the Sun $L_{st}$ can be calculated using the formula [14]:

$$L_{st} = L_s + C_s$$  \hspace{1cm} (6)

and Sun's true anomaly $V_s$ is:

$$V_s = M_s + C_s$$  \hspace{1cm} (7)

Avoiding significant error, the Latitude $\beta_s$ of the Sun can be considered zero as it remains on the ecliptic.

2.2 Coordinates System Conversion

The Sun's right ascension $\alpha_s$ and declination $\delta_s$ can be calculated by converting the Sun's elliptical coordinates $L_s$, using the following equations [15]:

$$\tan \alpha = \frac{\sin \lambda \cos \varepsilon - \tan \beta \sin \varepsilon}{\cos \lambda}$$  \hspace{1cm} (8)

$$\sin \delta = \sin \beta \cos \varepsilon + \cos \beta \sin \varepsilon \sin \alpha$$  \hspace{1cm} (9)

where: ($\varepsilon$) is the obliquity angle.

The mean obliquity angle of the ecliptic is given by the following formula which was adopted by the International Astronomical Union [16]:

$$\varepsilon = 23\cdot4333 - 46\cdot8150T_2 + 0.00059T_2^2 + 0.001813T_2^3$$  \hspace{1cm} (10)

where: $T_2$ is the number of Julian centuries from the epoch J2000.0 which can be calculated by equation 3.

The equatorial coordinate ($\delta, \alpha$) was converted to local horizontal coordinates ($A, a_l$) by using the following formulas [14, 15]:

$$\tan A = \frac{\sin H}{\cos H \sin \phi - \tan \delta \cos \phi}$$  \hspace{1cm} (11)

$$\sin a_l = \sin \phi \sin \delta + \cos \phi \cos \delta \cos H$$  \hspace{1cm} (12)

Where $\phi$ is the local geographical latitude

$H$ is the Hour angle.

$$e = 0.0167068364 - 0.000042037T_2 - 0.000001267T_2^2$$  \hspace{1cm} (13)

3. Calculating Sunrise, Sunset and Day length times

To calculate sunrise and sunset times, the steps below were followed [13]:

1. The equatorial coordinates ($\alpha, \delta$) for the Sun were given by equations 8, and 9.
2. The Hour angle of rising and setting was calculated by the following equation [13]:

$$H_o = \frac{\ell}{15} \cos^{-1} \left( - \tan \varphi \tan \delta \right) + \frac{\pi}{2}$$  \hspace{1cm} (14)

Where: $\delta$ is the declination

$\varphi$ is the geographical latitude.

$\ell$ is the geographical longitude.

The sidereal times of rising (S.T$_r$) and setting (S.T$_s$) were calculated as follows [14]:

$$S.T_r = 24 + \alpha_o - H_o$$  \hspace{1cm} (15)
\[ \text{S.T}_s = \alpha_o + H_o \]  
(16)

Where \( \alpha_o \) is the right ascension at rising or setting.

3. The corrections of refraction (R) at the moment of rising or setting were calculated according to Schaefer (1990) showed that the refraction values near the horizon fluctuated from 0.234° to 1.678°, while the total refraction varied over a range of R = 0.64° or 34.4 \[15\].

4. Correction of horizontal parallax at rising and setting was calculated and found to equal 8\(^\circ\).79 \[13\].

5. The correction of semi diameter at rising and setting for the Sun was calculated and found to equal 0.533 \[17\].

6. The total corrections at sunset or sunrise (\( X_{\text{sun}} \)) were calculated as:
\[ X_{\text{sun}} = 0^0.533 / 2 + 34^\circ.4 + 8^\circ.79 = 0^0.83560 \]  
(17)

7. The times of Sunrise (\( T_{\text{ro}} \)) and Sunset (\( T_{\text{so}} \)) with corrections in local sidereal time (LST) \[13\] were calculated as:
\[ T_{\text{ro}} = -\text{S.T}_r - X_s \]  
(18)
\[ T_{\text{so}} = -\text{S.T}_s + X_s \]  
(19)

8. The times from local sidereal time (LST) were converted to Greenwich mean time (GMT) by the following equations \[13\] :
\[ C = \text{int}[\left( \frac{\text{year} - 1}{100} \right)] \]
\[ Q_1 = \text{int}[365.22(\text{year} - 1)] + 428 + 1720994.5 + 2 - C + \text{int}\left( \frac{C}{4} \right) \]
\[ Q_1 = \frac{(Q_1 - 2415020)}{36525} \quad : \quad Q_2 = Q_1 \]
\[ R_1 = 6.6460656 + 2400.05126 \times 2Q_2 + 2.581 \times 10^{-5} \times Q_2^2 \]
\[ B_1 = 24 - [R - (24(\text{year} - 1900))] \]
\[ T_0 = 0.0657098D_1 - B_1 \]  
(20)
\[ GMT^{*}_{\text{ro}} = \left( T^{*}_{\text{ro}} - T_0 \right) \times 0.99727 \]
\[ GMT^{*}_{\text{so}} = \left( T^{*}_{\text{so}} - T_0 \right) \times 0.99727 \]  
(21)

9. The sunrise and sunset times were converted from Greenwich Mean Time (GMT) to Local Mean Time (LMT) + for east and – for west using the following equations \[10\]:
\[ \text{LMT}_r = GMT_{\text{ro}} + (L/15) \]
\[ \text{LMT}_s = GMT_{\text{so}} + (L/15) \]  
(22)

10. The day length is the interval time between sunrise (\( \text{LMT}_r \)) and sunset (\( \text{LMT}_s \)) and can be calculated by \[10\]:
\[ \text{Day length} = \text{LMT}_s - \text{LMT}_r \]  
(23)

4. Results and discussion

Computer programs were written using Visual Basic language to calculate the times of sunrise, sunset, and day length during one year for Baghdad city (Latitude = 33.34° N, Longitude = 44.43° E).

All the above calculations during 2019 depended on practical formulas, as in equations 1 to 23.

The results of sunrise, sunset, times, and variations between sunrise and sunset times with date in the year are shown in Figures-(2, 3). Based on these results, we could extract the following information:
1) The minimum time (Earliest) of sunrise in Baghdad was 4 h: 53 m from 5 Jun. to 20 Jun.
2) The maximum time (Latest) of sunrise in Baghdad 7 h: 07 m from 5 Jan. to 11 Jan.
3) The minimum time (Earliest) of sunset in Baghdad was 16 h: 55 m from 30 Nov. to 10 Dec.
4) The maximum time (Latest) of sunset in Baghdad was 19 h: 16 m from 25 Jun. to 5 Jul.

Figure 2-The variation time of Sunrise in Baghdad during the year 2019.

Figure 3-The variation time of Sunset in Baghdad during the year 2019.

The results of day length for Baghdad through the year 2019 as calculated by equation 23 are shown in Table-1. The results show that day length was the longest at the summer solstice in June and the shortest at the winter solstice in December. In addition, at equinoxes in March and September, the length of the day was about 12 hour.

The day length is the time between sunrise and sunset, as shown in Figure-4. Day length changes due to the change in sunrise time and sunset time throughout the year.
Table 1-The variations of day length period, in Baghdad during 2019

| Month: 1 Jan. | Day length h:m | Month: 2 Feb. | Day length h:m | Month: 3 Mar. | Day length h:m | Month: 4 Apr. | Day length h:m | Month: 5 May. | Day length h:m | Month: 6 Jun. | Day length h:m |
|---------------|----------------|---------------|----------------|---------------|----------------|---------------|----------------|---------------|----------------|---------------|----------------|
| 1             | 10:00          | 1             | 10:36          | 1             | 11:28          | 1             | 12:31          | 1             | 13:29          | 1             | 14:12          |
| 2             | 10:01          | 2             | 10:37          | 2             | 11:30          | 2             | 12:34          | 2             | 13:31          | 2             | 14:13          |
| 3             | 10:01          | 3             | 10:39          | 3             | 11:32          | 3             | 12:36          | 3             | 13:33          | 3             | 14:14          |
| 4             | 10:02          | 4             | 10:41          | 4             | 11:34          | 4             | 12:38          | 4             | 13:35          | 4             | 14:14          |
| 5             | 10:02          | 5             | 10:43          | 5             | 11:36          | 5             | 12:40          | 5             | 13:37          | 5             | 14:16          |
| 6             | 10:03          | 6             | 10:44          | 6             | 11:38          | 6             | 12:42          | 6             | 13:38          | 6             | 14:16          |
| 7             | 10:04          | 7             | 10:45          | 7             | 11:40          | 7             | 12:44          | 7             | 13:40          | 7             | 14:17          |
| 8             | 10:04          | 8             | 10:47          | 8             | 11:42          | 8             | 12:46          | 8             | 13:42          | 8             | 14:17          |
| 9             | 10:05          | 9             | 10:49          | 9             | 11:44          | 9             | 12:48          | 9             | 13:44          | 9             | 14:18          |
| 10            | 10:06          | 10            | 10:51          | 10            | 11:46          | 10            | 12:50          | 10            | 13:44          | 10            | 14:18          |
| 11            | 10:07          | 11            | 10:53          | 11            | 11:49          | 11            | 12:52          | 11            | 13:46          | 11            | 14:19          |
| 12            | 10:09          | 12            | 10:55          | 12            | 11:51          | 12            | 12:54          | 12            | 13:48          | 12            | 14:19          |
| 13            | 10:10          | 13            | 10:57          | 13            | 11:52          | 13            | 12:56          | 13            | 13:49          | 13            | 14:19          |
| 14            | 10:11          | 14            | 10:59          | 14            | 11:54          | 14            | 12:58          | 14            | 13:50          | 14            | 14:20          |
| 15            | 10:12          | 15            | 11:00          | 15            | 11:57          | 15            | 13:00          | 15            | 13:52          | 15            | 14:20          |
| 16            | 10:12          | 16            | 11:03          | 16            | 11:59          | 16            | 13:01          | 16            | 13:54          | 16            | 14:20          |
| 17            | 10:13          | 17            | 11:05          | 17            | 12:00          | 17            | 13:04          | 17            | 13:55          | 17            | 14:21          |
| 18            | 10:15          | 18            | 11:07          | 18            | 12:03          | 18            | 13:06          | 18            | 13:56          | 18            | 14:21          |
| 19            | 10:16          | 19            | 11:09          | 19            | 12:05          | 19            | 13:08          | 19            | 13:58          | 19            | 14:21          |
| 20            | 10:17          | 20            | 11:10          | 20            | 12:07          | 20            | 13:09          | 20            | 13:59          | 20            | 14:22          |
| 21            | 10:19          | 21            | 11:12          | 21            | 12:09          | 21            | 13:11          | 21            | 14:00          | 21            | 14:21          |
| 22            | 10:20          | 22            | 11:14          | 22            | 12:11          | 22            | 13:14          | 22            | 14:02          | 22            | 14:21          |
| 23            | 10:23          | 23            | 11:16          | 23            | 12:13          | 23            | 13:16          | 23            | 14:03          | 23            | 14:21          |
| 24            | 10:23          | 24            | 11:18          | 24            | 12:16          | 24            | 13:17          | 24            | 14:04          | 24            | 14:21          |
| 25            | 10:25          | 25            | 11:20          | 25            | 12:17          | 25            | 13:19          | 25            | 14:05          | 25            | 14:21          |
| 26            | 10:26          | 26            | 11:22          | 26            | 12:19          | 26            | 13:21          | 26            | 14:07          | 26            | 14:21          |
| 27            | 10:28          | 27            | 11:24          | 27            | 12:22          | 27            | 13:22          | 27            | 14:07          | 27            | 14:21          |
| 28            | 10:30          | 28            | 11:26          | 28            | 12:23          | 28            | 13:24          | 28            | 14:08          | 28            | 14:20          |
| 29            | 10:31          | 29            | 12:25          | 29            | 13:26          | 29            | 14:10          | 29            | 14:20          |               |               |
| 30            | 10:32          | 30            | 12:28          | 30            | 13:28          | 30            | 14:10          | 30            | 14:20          |               |               |

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| Month: 7 Jul. | Day length h:m | Month: 8 Aug. | Day length h:m | Month: 9 Sep. | Day length h:m | Month: 10 Oct. | Day length h:m | Month: 11 Nov. | Day length h:m | Month: 12 Dec. | Day length h:m |
|--------------|----------------|---------------|----------------|---------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| 1            | 14:19          | 1             | 13:48          | 1             | 12:52          | 1             | 11:52          | 1              | 10:51          | 1              | 10:07          |
| 2            | 14:19          | 2             | 13:46          | 2             | 12:50          | 2             | 11:50          | 2              | 10:50          | 2              | 10:07          |
| 3            | 14:18          | 3             | 13:43          | 3             | 12:48          | 3             | 11:47          | 3              | 10:48          | 3              | 10:06          |
| 4            | 14:18          | 4             | 13:45          | 4             | 12:46          | 4             | 11:45          | 4              | 10:46          | 4              | 10:05          |
| 5            | 14:17          | 5             | 13:41          | 5             | 12:45          | 5             | 11:44          | 5              | 10:44          | 5              | 10:04          |
| 6            | 14:16          | 6             | 13:39          | 6             | 12:42          | 6             | 11:42          | 6              | 10:42          | 6              | 10:03          |
| 7            | 14:15          | 7             | 13:38          | 7             | 12:41          | 7             | 11:39          | 7              | 10:40          | 7              | 10:03          |
| 8            | 14:15          | 8             | 13:36          | 8             | 12:39          | 8             | 11:38          | 8              | 10:39          | 8              | 10:02          |
| 9            | 14:14          | 9             | 13:34          | 9             | 12:36          | 9             | 11:36          | 9              | 10:37          | 9              | 10:01          |
| 10           | 14:14         | 10            | 13:32          | 10            | 12:35          | 10            | 11:33          | 10             | 10:35          | 10             | 10:00          |
| 11           | 14:12         | 11            | 13:31          | 11            | 12:32          | 11            | 11:31          | 11             | 10:35          | 11             | 10:00          |
| 12           | 14:12         | 12            | 13:29          | 12            | 12:30          | 12            | 11:30          | 12             | 10:33          | 12             | 10:00          |
| 13           | 14:11         | 13            | 13:27          | 13            | 12:29          | 13            | 11:28          | 13             | 10:31          | 13             | 09:59          |
| 14           | 14:10         | 14            | 13:26          | 14            | 12:26          | 14            | 11:25          | 14             | 10:30          | 14             | 09:58          |
| 15           | 14:09         | 15            | 13:24          | 15            | 12:24          | 15            | 11:25          | 15             | 10:28          | 15             | 09:59          |
| 16           | 14:08         | 16            | 13:22          | 16            | 12:23          | 16            | 11:22          | 16             | 10:26          | 16             | 09:58          |
| 17           | 14:07         | 17            | 13:21          | 17            | 12:20          | 17            | 11:20          | 17             | 10:25          | 17             | 09:58          |
| 18           | 14:06         | 18            | 13:19          | 18            | 12:18          | 18            | 11:18          | 18             | 10:23          | 18             | 09:58          |
| 19           | 14:05         | 19            | 13:17          | 19            | 12:17          | 19            | 11:16          | 19             | 10:22          | 19             | 09:57          |
| 20           | 14:04         | 20            | 13:16          | 20            | 12:14          | 20            | 11:13          | 20             | 10:20          | 20             | 09:58          |
| 21           | 14:02         | 21            | 13:13          | 21            | 12:12          | 21            | 11:12          | 21             | 10:19          | 21             | 09:57          |
| 22           | 14:02         | 22            | 13:11          | 22            | 12:10          | 22            | 11:10          | 22             | 10:18          | 22             | 09:57          |
| 23           | 14:00         | 23            | 13:10          | 23            | 12:08          | 23            | 11:08          | 23             | 10:17          | 23             | 09:57          |
| 24           | 13:58         | 24            | 13:08          | 24            | 12:06          | 24            | 11:06          | 24             | 10:16          | 24             | 09:57          |
| 25           | 13:58         | 25            | 13:06          | 25            | 12:04          | 25            | 11:04          | 25             | 10:14          | 25             | 09:57          |
| 26           | 13:56         | 26            | 13:03          | 26            | 12:02          | 26            | 11:03          | 26             | 10:13          | 26             | 09:58          |
| 27           | 13:54         | 27            | 13:02          | 27            | 12:00          | 27            | 11:01          | 27             | 10:12          | 27             | 09:58          |
| 28           | 13:54         | 28            | 13:00          | 28            | 11:58          | 28            | 10:59          | 28             | 10:11          | 28             | 09:58          |
| 29           | 13:52         | 29            | 12:58          | 29            | 11:56          | 29            | 10:57          | 29             | 10:10          | 29             | 09:59          |
| 30           | 13:50         | 30            | 12:56          | 30            | 11:53          | 30            | 10:55          | 30             | 10:08          | 30             | 09:59          |
| 31           | 13:48         | 31            | 12:54          | 31            | 10:53          | 31            | 10:53          | 31             | 09:59          | 31             | 09:59          |
Figure-5 represents the variation of day length periods in Baghdad during 2019, from which we can conclude the following information:

1. The minimum period of day length in Baghdad was 9$^{h}$: 57$^{m}$ at 17 Dec.
2. The maximum period of day length in Baghdad was 14$^{h}$: 22$^{m}$ at 20 Jun.

The day length is the time between sunrise and sunset.

The length of the day is a function of the latitude only (longitude has no effect on day length), in addition to the day of the year. The variations in day length period as a function of latitudes (0°, 15°N, 30°N, 45°N, 60°N) during 2019 is shown in Figure-6.

From Figure-6, the day length at the equinoxes (21 March and 23 September) was equal, regardless of latitude. Thus it could be observed that summer days in higher latitudes (45°N, 60°N) were longer than those in lower latitudes (15°N, 30°N) and that winter days were shorter.

The equator area (latitude 0°) had less variation (two minutes only) in day length throughout the year 2019, as shown in Table-2.
Figure 5-The variation of day length period as a function of latitudes (0°, 15N, 30N, 45N, 60N) during 2019.

Table 2-The maxim and minim day length period for latitudes (0°, 15N, 30N, 45N, 60N) during 2019.

| Latitudes   | L=0    | L=15N  | L=30N  | L=45N  | L=60N  |
|-------------|--------|--------|--------|--------|--------|
| **Longer day** | 12 h:08 m | 13 h:01 m | 14 h:05 m | 15 h:37 m | 18 h:52 m |
| **Shorter day** | 12 h:06 m | 11 h:14 m | 10 h:13 m | 08 h:46 m | 05 h:52 m |
| **Variation**   | 00 h:02 m | 01 h:47 m | 03 h:52 m | 06 h:51 m | 13 h:00 m |

5. Conclusions
The main conclusions from this study could be summarized as follows:
1. The variation range of sunrise time in Baghdad was between 4 h:53 m and 7 h:07 m, and the variation time was equal to 2 h:14 m = 134 m during the year.
2. The variation range of sunset time was between 16 h:55 m and 19 h:16 m, and the variation time was equal to 2 h:21 m = 141 m during the year.
3. The variation range in the periods of day length in Baghdad was between 9 h:57 m and 14 h:22 m, and the variation time was equal to 4 h:25 m = 265 m during the year.
4. The longer variation of day length was recorded in the latitudes 0°, 15N, 30N, 45N, and 60N during 2019, with a range between 12 h:06 m and 5 h:52 m).
5. The shorter variation of day length was recorded in latitudes 0°, 15N, 30N, 45N, and 60N) during 2019, with a range between 12 h:08 m and 18 h:52 m).
6. The period of day length recorded in latitudes 0°, 15N, 30N, 45N, and 60N at the equinoxes (21 March and 23 September) was equal to 12 h.
7. The area near the poles (above latitude 66.5N) had no regular behavior as related to day length.
8. The same behavior for day length applies to the corresponding southern latitudes.

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