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Influence of metallic nanoparticles on upconversion processes

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It is well known that Raman scattering and fluorescence can be enhanced by the presence of metallic nanoparticles. Here, we derive simple equations to analyze the influence of metallic nanoparticles on upconversion processes such as nonradiative energy transfer or excited state absorption. We compare the resulting expressions with the more familiar Raman and fluorescence cases and find significant differences. We use numerical simulations to calculate the upconverted signal enhancement achievable by means of metallic spheres of different radii and find particles of 100–400 nm radius at infrared frequencies to be favorable. We also discuss the considerable challenges involved in using metallic particles to enhance upconversion for solar energy. © 2009 American Institute of Physics. [DOI: 10.1063/1.3075848]

I. INTRODUCTION

Upconversion processes allow to obtain photons of energy significantly larger than the excitation and are present, for example, in many different rare-earth systems. Potential applications include lasers, three dimensional imaging, quantum counters, or photovoltaic cells. A usual path to maximize the upconversion emission efficiency consists in trying different combinations of host matrices and rare-earth atoms. The crystal field from the host influences the transition probabilities between the rare-earth levels in a manner very dependent on the microscopic details of the quantum charge distributions.

An alternative possibility, of interest here, relies on the possibility to locally enhance the excitation strength using metallic nanoparticles as local optical antennas. In addition, the decay rates of a given quantum emitter also depend on the environment, from purely electromagnetic, macroscopic mechanisms which are often predominant in systems consisting of rare earths such as erbium or erbium-ytterbium: excited state absorption (ESA) and nonradiative energy transfer (NRET). One reason for optimism in the search of large signal enhancements is the proportionality between the upconverted signal far from saturation and the square of the light intensity. This reminds of the well-known fourth power relation between the Raman signal and the local electric field enhancement. Thus, one could expect upconversion gains from localized plasmonic resonances as large as for SERS. Large enhancements are, however, far from guaranteed, as both NRET and ESA differ

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from Raman in an essential property. Like fluorescence, they are incoherent absorption-emission processes, which can be treated using rate equations, not a coherent scattering formalism. In other words, they involve real, not virtual, transitions.

We derive simple analytical equations to study the influence of the environment on upconversion processes. We also present similar equations for Raman scattering and fluorescence in order to compare the different processes. Our main objective is to obtain simple equations that capture the essence of the influence of nanoantennas on these processes. Thus, we use simplified level schemes and ignore some of the very complex physical phenomena that can enter in a real system. We illustrate the physical content of our model using numerical simulations of metallic particles of different sizes at wavelengths where they exhibit localized surface plasmon polariton resonances. We also briefly consider how differences on the level scheme translate into the enhancement of the upconversion signal (see Appendix B).

II. MODEL AND NOTATION

As Fig. 1(a) illustrates, we begin by studying a very general case, how particles imbedded in an homogeneous, lossless medium affect the light emitted by quantum emitters with discrete energy levels—atoms, molecules, quantum dots, etc. The energy level schemes in Figs. 1(b)–1(e) illustrate the different emission processes of interest, Raman, fluorescence, NRET, and ESA.

An experimental upconversion system can present a very complex energy level scheme, with the different transition rates—of possible electric dipolar, magnetic dipolar, or even electric quadrupolar character—very sensitive to the exact microscopic details of the sample. To avoid considering so many variables, some of them not necessarily known, we consider only dipolar electric transitions and relatively simple schemes that illustrate many of the phenomena of interest. We leave to Appendix B a further discussion of possible changes on the level scheme.

We study the low intensity regime so that there are no saturation effects. We focus on the influence of purely electromagnetic effects that result directly from the presence of the metallic nanoparticles. We do not consider, for example, possible changes on the crystal field due to the presence of the particle. As we consider single, fixed quantum emitters, diffusion effects which are often important for rare-earth systems do not play a role. Nonlocal effects on the dielectric constant can in principle increase the nonradiative decay rate and thus diminish the emitted power. They are predominant at short distances to the substrate, but they will be significantly less important at the conditions of maximum upconversion enhancement shown in the following and we have not considered them. We also assume that the particle resonance is not modified by the presence of the rare-earth emitters.

For real systems, it will be necessary to match the particle resonances, the excitation frequency, and the energy levels. To facilitate comparison over a broad range of excitation frequency $\omega_{\text{exc}}$, the energy difference between the ground and first excited state is always matched to the incident light, and other energy differences scale directly with this value. The excitation is assumed broad enough for population equations to be applicable and for frequency shifts due to the environment to be negligible, but sufficiently narrow to excite only the desired transition. The magnitude of interest is the ratio between the light power emitted in all directions at the desired frequency $\omega_{\text{out}}$ with and without the particles $P_{\text{out}}/P^{0}$.

III. ANALYTICAL EXPRESSIONS

We introduce in this section the equations describing the effect of the particle on the emitted power $P_{\text{out}}/P^{0}$, for upconversion, both for ESA and NRET, as also for the known cases of fluorescence and Raman emission. Appendix A presents a more complete discussion on how to derive the equations and the corresponding assumptions.

A. Raman scattering

We start with a short derivation of the well-known electromagnetic contribution to SERS. Raman is a coherent process in which incident and scattered photons differ by a small energy amount that can be transferred, e.g., to a vibrational level of a molecule. The scattering enhancement is partly due to the enhancement of the local intensity at the scatterer position and partly due to the enhancement of the radiation emission due to the presence of the nanoantenna (Appendix A). The former is characterized by the enhancement $K_{01}$ of the projection of the field into the dipole. The indices stand for the frequency $\hbar \omega_{\text{in}}=E_{1}-E_{0}$ of the field that matches a transition between two levels. The energy levels correspond to the excitation and emitted energy according to the simplified scheme in Fig. 1(b). The photon emission is characterized by the radiative rate $\Gamma_{1f}^{R}$ in the presence of the nanoantenna, and $\Gamma_{1f}^{R0}$ without antenna, at the emission frequency $\hbar \omega_{\text{out}}=E_{1}-E_{f}$. The ratio of power emitted in all directions with and without nanoparticle is then given by

$$\frac{P_{\text{out}}}{P^{0}} = \left|K_{01}\right|^{2} \frac{\Gamma_{1f}^{R}}{\Gamma_{1f}^{R0}}. \tag{1}$$
We discuss in Appendix A how in occasions $|K_{01}|^2 \sim \Gamma_0^R/\Gamma_{10}^R$. The equality holds, for example, in the particular case of a confocal setup. If the excitation and emission frequency are sufficiently close, we finally find

$$\frac{P_{\text{out}}}{P^0} \sim |K_{01}|^4.$$  \hfill (2)

The often discussed proportionality between the intensity of the emitted light and the fourth power of the field enhancement follows from such frequently encountered conditions. It is a direct consequence of the coherent character of the process, not of the particularities of Raman, and also characterizes elastic (Rayleigh) scattering.

\section*{B. Fluorescence}

Fluorescence is very different from the scattering case as the former involves a real transition, and can thus be described by population equations. Introducing at this state the notation for fluorescence and up-conversion, $K_{ml}$ gives as before the near-field enhancement along the dipole orientation between levels $|m\rangle$ and $|l\rangle$. $\Gamma_{ml}^T$ is the total decay rate between the levels and is the sum of three contributions $\Gamma_{ml}^T = (\Gamma_{ml}^R + \Gamma_{ml}^{NR} + \Gamma_{ml}^{R0})$ that represent, respectively, the radiative decay resulting in photon emission, the nonradiative decay due to a transfer of energy to the particle, and the nonradiative intrinsic decay due to internal transitions in the quantum emitter. Neither the process described by $\Gamma_{ml}^{R0}$ nor by $\Gamma_{ml}^{NR}$ result in photon emission to the far field, and the energy is lost, for example, as heat. The quantum yield $\eta_{ml} = \Gamma_{ml}^R / (\Sigma_m \Gamma_{ml}^T)$ is the fraction of quantum emitters in level $|m\rangle$ that decay directly to $|l\rangle$ by emitting a photon detectable in the far field at frequency $\omega_{ml}$. The sum over levels $n$ serves to include formally cases in which the quantum emitter can decay from $|m\rangle$ to levels other than $|l\rangle$. We note $\Gamma_{m0}^T$, $\Gamma_{m0}^{R0}$ and $\eta_{m0}$ for the values in the homogeneous medium, in the absence of any particle ($\Gamma_{m0}^{NR} = 0$ by definition).

In Fig. 1(c), a quantum emitter is excited to $|1\rangle$, from which it decays to the fluorescent level $|j\rangle$ before returning to the ground state $|0\rangle$. Appendix A shows that population equations allow to account for the absorption and for the radiative and nonradiative processes and to derive the population of $|j\rangle$. The quantum emitter decays from this level back to the ground state $|0\rangle$ with or without photon emission, as described by $\eta_{j0}$. Finally, the comparison of the fluorescent signals with and without nanoparticle in the low intensity illumination regime under constant illumination yields the known equation

$$\frac{P_{\text{out}}}{P^0} = |K_{01}|^4 \frac{\eta_{j0}}{\eta_{j0}},$$  \hfill (3)

which only depends on the near-field enhancement and the ratio between the quantum yields with and without particles. A key difference with scattering is that for each excitation of the quantum emitter to $|1\rangle$ a maximum of one photon contribute to the fluorescence. Only after the quantum emitter has decayed a new excitation and subsequent photon emission can occur, and the number of the excited molecules is always lower than the total number of quantum emitters.

Such limitation does not exist in scattering processes. If $k_{10}^{NR} = 0$, the quantum yield for homogeneous, lossless media $\eta_{j0}$ is equal to one and the signal enhancement is lower than $|K_{01}|^2$, equal if the particles do not introduce nonradiative losses.

\section*{C. Upconversion: ESA}

Moving to discuss upconversion processes, we consider in this section the simple energy level schemes illustrated in Figs. 1(d) and 1(e). In ESA, a first photon excites a quantum emitter from level $|0\rangle$ to $|1\rangle$ and a second excites this quantum emitter to $|2\rangle$. The energy of the emitted photon due to the $|2\rangle \rightarrow |0\rangle$ transition is here exactly twice the corresponding value for the incident photons, which is not necessarily the case for more complicated level schemes.

Proceeding similarly as before, we obtain in Appendix A for the upconverted signal at $\omega_{out}$

$$\frac{P_{\text{out}}}{P^0} = |K_{01}|^4 \frac{\Gamma_{10}^R / \Gamma_{10}^{R0}}{\eta_{j0} / \eta_{j0}}.$$  \hfill (4)

If $\Gamma_{21}^R = 0$, the already introduced relationship $\Gamma_{10}^R / \Gamma_{10}^{R0} = |K_{01}|^2$ is verified and there is no intrinsic losses, $P_{\text{out}}/P^0 \leq |K_{01}|^2$, equal in the absence of nonradiative decay. Under such conditions, the enhancement from ESA and fluorescence are similar.

\section*{D. Upconversion: NRET}

The scheme in Fig. 1(e) represents the considered level scheme for NRET. The energy transferred nonradiatively from the relaxation of the two-level quantum system $x$ according to the transition $|1\rangle \rightarrow |0\rangle$ serves to excite the three-level quantum system $y$ from level $|1\rangle$ to $|2\rangle$.

Solving the equations in Appendix A, we obtain for the upconverted signal from the transition $|2\rangle \rightarrow |0\rangle$ of the quantum system $y$,

$$\frac{P_{\text{out}}}{P^0} = |K_{01}|^4 \frac{(\eta_{10}^{eq} / \Gamma_{10}^{R0})^2}{\eta_{20}^{eq} / \eta_{10}^{eq}}.$$  \hfill (5)

where we ignore any change in the efficiency of the NRET process due to the particle. We have also assumed identical field enhancement for $x$ and $y$ and an effective decay rate $\Gamma_{10}^R$ for the complete system that is affected by the particle in the same way as for an individual quantum emitter. If there is no intrinsic losses, $y$ decays directly from $|2\rangle$ to $|0\rangle$ and $|K_{01}|^2 = \Gamma_{10}^R / \Gamma_{10}^{R0}$ the presence of the particles cannot increase the emission of upconverted photons.

We observe that the obtained expressions for the two upconverted processes are proportional to the fourth power of the near-field enhancement, similarly to the usual expression for Raman signal. However, the fourth power arises in upconversion because it is a two-photon process, while in Raman it emerges from a similar contribution from the near-field enhancement and the emission efficiency of the dipole in Eq. (1). Also, the upconversion processes involve real transitions as for fluorescence. Thus, when writing population equations, nonradiative relaxation terms are introduced, and the interplay between intrinsic losses and radiative and
nonradiative decay rates plays a key role. Due to these terms, we expect weaker enhancements for upconversion than for Raman scattering. In what follows, we shall analyze this interplay by modeling rigorously the electromagnetic interaction with a metallic nanoparticle.

IV. RESULTS

We study next light emission in the proximity of a spherical metallic particle embedded in glass (with dielectric constant $\varepsilon_{\text{glass}}=2.25$). We consider (Fig. 2) dipolar excitation and emission parallel to the incident electric field vector $\vec{E}^0$ and perpendicular to the propagation direction $\vec{k}$ with two orientations, one pointing toward the center of the particle (radial orientation) and the other tangential to the sphere (tangential orientation). The quantum emitter is in the plane parallel to $\vec{E}^0$ and $\vec{k}$ and containing the center of the sphere, at a distance to the sphere surface $d$. For a sufficiently small particle, the total resulting electric fields are exactly parallel to $\vec{E}^0$ for both orientations of the dipole. For larger particles we still consider the transition to be only sensitive to the component parallel to $\vec{E}^0$.

We use numerical simulations to calculate the relevant parameters entering the power emission model: the enhancement factor and the modification of the radiative and nonradiative decay rates in the presence of the particle. We then derive the modification of power radiated by the emitter in the different scenarios, Raman, fluorescence, and the two upconversion processes.

The simulations use a multiple multipole method (MAX-1) to solve the Maxwell equations. It is a semianalytical method where the electromagnetic field is expanded by a series of basis fields called expansions. Each of the expansions is an analytical solution of the field equations within a homogeneous domain. The decomposition of the field is numerically optimized to minimize the error at the boundary conditions. The cross section of the quantum emitter is considered small enough not to affect the near fields of the resonant sphere. The average error is smaller than 0.1%, often much smaller, and an ~25% decrease in the number of orders of the expansions does not significantly affect the results. The dielectric constants are taken from Palik.37

A. Decay rates and near-field enhancement

Let us first focus on the influence of both the distance to the surface $d$ and the wavelength on the parameters entering the analytical expressions for the emitted power: the field enhancement $K$, the field enhancement $K$, the field enhancement $K$, and the radiative and nonradiative rates, $\Gamma^{R}, \Gamma^{R0}, \Gamma^{NR}, \Gamma^{NR0}$; the wavelength refers to the excitation, for the enhancement and to the emission, for the decay rates.

Figure 3 illustrates the distance and wavelength dependence of those parameters for the 100 nm radius silver sphere and radial orientation. It is useful for the discussion to also plot the quantum yield, with $k^{NR}=0$. The dipolar resonance is discernible in the near-field enhancement of ~4 at around 1200 nm [Fig. 3(a)]. This wavelength is significantly shifted to the red of the small particle value due to the non-negligible size.38 We can also observe at least one higher order resonance at shorter wavelengths (around 450 nm). The change on radiative decay rate $\Gamma^R/\Gamma^{R0}$ shown in Fig. 3(b) exhibits a similar behavior as the enhancement, with a broad maximum near 1200 nm; in particular, near this maximum $\Gamma^R/\Gamma^{R0}\sim|\vec{k}|^2$ as previously discussed. At shorter wavelengths the signature of not just one, but two higher order resonances are discernible. In contrast, the nonradiative decay rate change $\Gamma^{NR}/\Gamma^{R0}$ [Fig. 3(c)] behaves very differently, with a very marked maximum near 350 nm up to three orders of magnitude larger than the corresponding maximum for the radiative decay rate. $\Gamma^{NR}/\Gamma^{R0}$ also increases significantly for small distances to the substrate. The conditions under which $\Gamma^{NR}/\Gamma^{R0}$ is significantly larger than $\Gamma^{R}/\Gamma^{R0}$ can clearly be seen on Fig. 3(d) when the quantum yield tends to zero. It happens for wavelengths around 350 nm and at small distances.

The size of the particle can greatly influence the results. This is illustrated in Figs. 4(a)–4(c) where the wavelength dependence for changing radius and fixed distance to the surface $d=2$ nm are studied. If we concentrate on the diplo-
lunar resonance corresponding to the first near-field enhancement and radiative decay rate maximum starting from the longer wavelengths, we observe a shift to the red for increasing radii. Furthermore, the peak becomes weaker and broader, with the maximum near-field enhancement remaining larger than 3.5 also for 400 nm radius particles. The nonradiative rate change behaves again differently than the radiative and nonradiative decay rates for the radial, nontangential, symmetrical orientation and for tangential orientation and silver particle.

B. Signal enhancement

Let us study now how the near-field enhancement and the modification of the radiative and nonradiative decay rates by the spherical particle affect the emitted power \( P_{\text{emitted}} \) for the different mechanisms of Raman scattering [Eq. (1)], fluorescence [Eq. (3)], ESA upconversion process [Eq. (4)], and NRET upconversion process [Eq. (5)]. To simplify, at this stage \( \kappa^{NR}=0 \) for all involved transitions and, for ESA and NRET, the decay \( |2\rangle \rightarrow |1\rangle \) is negligible. To be able to study the evolution over a large wavelength range, we consider that the transition \( |0\rangle \rightarrow |1\rangle \) (and \( |1\rangle \rightarrow |2\rangle \)) coincides with the excitation frequency. The transitions \( |1\rangle \rightarrow |f\rangle \) and \( |i\rangle \rightarrow |0\rangle \) correspond to 0.95 and 0.8 times the excitation frequency for the Raman and the fluorescence level schemes, correspondingly. We discuss the results as a function of the excitation frequency.

We start discussing the results for a 100 nm silver sphere and radial orientation (Fig. 5), if not otherwise mentioned. For Raman [Fig. 5(a)], the presence of a simple metallic particle yields an enhancement of more than two orders of magnitude, with a broad maximum for the dipolar resonance and close distances to the particle. An enhancement of almost four orders of magnitude is possible at 2 nm distance for 10 nm radius. As expected, the Raman signal relates closely to the near-field enhancement (Figs. 3 and 4). An enhancement is also possible for fluorescence [Fig. 5(b)], but significantly weaker than for Raman because it depends on the square of the near-field enhancement, not the fourth power, and because there is a competition between this enhancement and the quenching of the emitter.

For the ESA case, as seen in Fig. 5(c), the signal is low at small distances to the surface \( d \) due to the quenching of the emitter. The signal is also especially low for excitation frequencies around \( \sim 350 \) nm where the nonradiative decay rate for the \( |1\rangle \rightarrow |0\rangle \) predominates, and at around \( \sim 700 \) nm, which coincides with strong nonradiative decay rate and thus low quantum yield at the upconverted frequency. Related to the discussion in the previous sections, we observe that the fluorescence and ESA enhancement look quite similar and both exhibit a maximum of 8–9 at the dipolar frequency. Considering a 10 nm sphere [insert in Figs. 5(b) and 6(a)] serves to demonstrate that the similitude is not universal.

The results are very different for NRET as seen in Fig. 5(d). Indeed, the most striking feature for NRET is the very small maximum signal increase (only slightly larger than 1) in the presence of the particle. The increase appears at significant distances to the surface, i.e., where the particle influence is small. The dissimilarity with ESA signal is due to...
Unsurprisingly from the results of Sec. IV A, the 100 nm gold spheres for radial orientation behave very similarly to their silver counterpart [Fig. 6(e)]. Last, for the 100 nm silver sphere and tangential orientation [Fig. 6(f)], it is only possible to obtain a weak ESA signal enhancement of $\sim 2$. This reminds recent studies of fluorescence which point to the convenience of radial orientation.\textsuperscript{19} In contrast, for NRET, wavelengths close to 1150 nm and distances of $\sim 60$ nm we obtain an enhancement of $\sim 3.5$ for tangential orientation, \textit{larger} than for radial orientation in the same conditions [Fig. 5(d) and insert in Fig. 6(f)]. It is also larger than the values for ESA and tangential orientation [Fig. 6(f)], which is a consequence of the term $\Gamma^{\text{NR}}_{10}/\Gamma^{\text{R}}_{10}$ being larger than 1, i.e., the total decay rate of the transition decreasing under those conditions.

We have obtained a maximum enhancement of the upconverted signal for large particles on the $\sim 100-400$ nm radius range, for wavelengths of $\sim 1$ to a few micrometers. The enhancement is about $\sim 8$ for ESA and radial orientation. The maximum position is at infrared frequencies and for a distance of a few tens of nanometers to the surface. Significantly, for large particles the maxima for $\Gamma_{10}/\Gamma^{\text{R}}_{10}$ and the near-field enhancement are not at the same frequency, which allows to favor one over the other. Changing the shape of the particle, or using several particles, should allow a similar effect also for smaller dimensions.\textsuperscript{42} For NRET, we obtained a maximum enhancement of $\sim 3.5$ for tangential orientation.

We emphasize that this study is mostly concerned by the emission of a single quantum emitter, which could be useful, for example, for near-field imaging or to characterize individual light sources. If the objective is to use upconversion for solar applications, the question of efficiency becomes crucial. In that case, one should also consider the fact that metallic particles not only enhance the field but also absorb the incident radiation. For example, we consider an absorption cross section between levels $|0\rangle$ and $|1\rangle$ $g_{01}^\text{abs}$ \textasciitilde $10^{-20}$ cm$^{-2}$, and that a 2\% of the quantum emitters in level $|1\rangle$ are excited to $|2\rangle$ and result in an upconverted photon. In the presence of the resonant spheres and ignoring saturation, an enhancement of $\sim 10$ can be obtained resulting in an effective cross section for upconversion $\sim 10 \times 0.02 \times 10^{-20}$ \textasciitilde $210^{-21}$ cm$^{-2}$. This must be compared to the absorption cross section of the particle. For a size parameter larger than 1, we use the geometrical cross section for a rough estimation of the scattering cross section of a 100 nm radius sphere particle and obtain $\sim \pi 10^{-10}$ cm$^{-2}$. The simulation results give an absorption cross section of $\sim 2.5 \times 10^{-11}$ cm$^{-2}$ at 1200 nm. If we consider that all quantum emitters result in the maximum increase—no averaging over distance and orientation or considering interactions between the emitters and with the particles—it is still necessary to have $10^{10}$ rare-earth atoms per particle to reach a similar number of upconverted photons than absorbed by the particle. For an homogeneous distribution between 0 and 100 nm, an unrealistic concentration of quantum emitters of $\sim 4 \times 10^{23}$ cm$^{-3}$ is required.
V. CONCLUSION

To summarize, we have derived equations that give insight on how the emission from upconverted media behaves in the presence of nanoparticles, and we have compared them with fluorescence and Raman emission. Although the emission depends on the fourth power of the local field, the detailed analysis reveals typical gains much weaker than for Raman. It is sometimes similar but can also be significantly smaller than for fluorescence. We obtain moderate enhancement of the upconverted signal when using large metallic particles illuminated in the infrared. We discuss the possibility of larger signal enhancements for more complex systems (see Appendix B). Using more complex resonant geometries can also be useful to obtain strong upconversion signal. For example, dielectric antennas can result in strong near fields without quenching.43

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APPENDIX A: DERIVATION OF THE ANALYTICAL EXPRESSIONS

1. Raman scattering

In this section, we derive the form of the enhancement of the scattered field produced by a nanoantenna. Let us consider a system where the excitation and the detection are produced by a source located at point \( \mathbf{r}_1 \). We characterize the source by an electric dipole moment \( \mathbf{p}_1 = p_1 \mathbf{u} \), where \( \mathbf{u} \) is a unit vector that describes the polarization of the source. The electric field produced at \( \mathbf{r} \) reads

\[
\mathbf{E}(\mathbf{r}) = \tilde{\mathbf{G}}(\mathbf{r}, \mathbf{r}_1, \omega_{in})\mathbf{p}_1, \tag{A1}
\]

where \( \tilde{\mathbf{G}} \) denotes Green’s tensor of the system at the excitation frequency \( \omega_{in} \). This is simply the most general linear relation between two vectors. If the emitter is in a vacuum, then Green’s tensor is the vacuum Green’s tensor \( \tilde{\mathbf{G}}_0 \). If the system includes a confocal microscope or any linear optical system, Green’s tensor accounts for it. Thus, although we have introduced a dipole source, a variety of illumination conditions is included formally. In the presence of a nanoantenna, Green’s tensor can be cast in the form

\[
\mathbf{E}(\mathbf{r}) = [\tilde{\mathbf{G}}_0(\mathbf{r}, \mathbf{r}_1, \omega_{in}) + \tilde{\mathbf{S}}(\mathbf{r}, \mathbf{r}_1, \omega_{in})]\mathbf{p}_1, \tag{A2}
\]

where \( \tilde{\mathbf{S}} \) accounts for the contribution of the nanoantenna to Green’s tensor. If we compare the field along \( \mathbf{v} \) at \( \mathbf{r} \) with and without the nanoantenna, we find an enhancement \( K_{\omega_{in}} \) given by

\[
K_{\omega_{in}} = \frac{\mathbf{v} \cdot \tilde{\mathbf{G}}(\mathbf{r}, \mathbf{r}_1, \omega_{in})\mathbf{u}}{\mathbf{v} \cdot \tilde{\mathbf{G}}_0(\mathbf{r}, \mathbf{r}_1, \omega_{in})\mathbf{u}}. \tag{A3}
\]

The field induces a dipole moment along \( \mathbf{v} \) given by

\[
\mathbf{p}_2 = p_2 \mathbf{v} = \mathbf{v}[\alpha \mathbf{e}_0 \mathbf{v} \cdot \mathbf{E}(\mathbf{r})], \tag{A4}
\]

where \( \alpha \) is the polarizability. It is either at the same frequency for Rayleigh scattering or at a slightly different frequency for Raman scattering \( \omega_{out} \). The field produced by the induced dipole at a point \( \mathbf{r}' \) is given by

\[
\mathbf{E}(\mathbf{r}') = \tilde{\mathbf{G}}(\mathbf{r}', \mathbf{r}_1, \omega_{out})\mathbf{p}_2, \tag{A5}
\]

We now consider two cases. The case where we have a confocal detection system and the other case we are interested in the emission over a given solid angle. Let us first assume that we use a confocal detection system with both illumination and detection at the same point \( \mathbf{r}' = \mathbf{r}_1 \). We further assume that before detection light passes through a polarizer parallel to the unit vector \( \mathbf{u} \). The signal is then proportional to

\[
P_{\text{out}} \propto |\mathbf{u} \cdot \mathbf{E}(\mathbf{r})|^2 = |\mathbf{u} \cdot \tilde{\mathbf{G}}(\mathbf{r}_1, \mathbf{r}_1, \omega_{out})\mathbf{p}_2|^2, \tag{A6}
\]

if we now compare the signal \( P_{\text{out}} \) obtained in the presence of the nanoantenna with the signal \( P^0 \) without nanoantenna, we get

\[
\frac{P_{\text{out}}}{P^0} = \frac{|\mathbf{v} \cdot \tilde{\mathbf{G}}(\mathbf{r}_1, \mathbf{r}_1, \omega_{in})\mathbf{p}_1|^2}{|\mathbf{v} \cdot \tilde{\mathbf{G}}_0(\mathbf{r}_1, \mathbf{r}_1, \omega_{in})\mathbf{p}_1|^2} = K_{\omega_{in}}^4. \tag{A7}
\]

The equation also holds for Raman if the difference between emission and excitation frequency is sufficiently small. The exponent of 4 shows that the signal varies like the fourth power of the enhancement produced by the presence of the antenna. The derivation shows that the fourth power enhancement is due to the role of the antenna that enhances both the illumination and the emission. Note that we have assumed that the detection is made at the same point and for the same polarization than the illumination. A different configuration might not yield this fourth power of the enhancement.

In particular, we now consider that the detection system integrates over a solid angle \( \Omega \). We denote \( \Omega_{\text{out}}^{\text{RR}} \) the emission rate of a dipole in the presence of the nanoantenna and \( \Omega_{\text{out}}^{\text{R0}} \) the emission rate without the nanoantenna. The emission rate refers here to the photons emitted through a surface subtending a solid angle \( \Omega \). The enhancement of the Raman process is then given by

\[
\frac{\Omega_{\text{out}}^{\text{RR}}}{\Omega_{\text{out}}^{\text{R0}}} = K_{\omega_{in}}^4. \tag{A8}
\]
We have simply written here that the amplitude of the induced dipole is enhanced by a factor \( K \) and that its emission in a given solid angle is enhanced by a factor \( K_{\text{em}} \). If we are interested in the emission over all directions, we simply use the corresponding radiative rate denoted by \( \Gamma_{\text{em}} \), which is the case in the text. Note that in the case that the emission pattern is not far from isotropic and is predominantly polarized as the excitation we have due to reciprocity \( |K|^2 \sim \frac{\Omega}{\Gamma_{\text{em}}^2} \), a relationship that we have used in the text to obtain simplified equations; for \( \omega_{\text{em}} \sim \omega_{\text{out}} \), the fourth power \( |K_{\text{em}}|^4 \) is also under such conditions a good approximation for emission over all directions.

### 2. Fluorescence scattering

We present here the known derivation of the fluorescence equation to get familiar with the procedure followed for the upconversion expressions. As it involves a real transition, the derivation used for the Raman case is not valid. For weak illumination, the power emitted at the fluorescence frequency is due to spontaneous emission and is proportional to \( N_r \), the population of the excited state. We write population equations for the different levels in order to derive the population of the excited state in stationary regime under constant illumination. The incident light excites the quantum emitter from state \( |0\rangle \) to state \( |1\rangle \), with subsequent relaxation to \( |0\rangle \) [Fig. 1(c)]. The different processes are absorption, radiative relaxation, and nonradiative relaxation. As before, \( \Gamma_{\text{m0}}^R \) describe the radiative decay rate between \( |m\rangle \) and \( |l\rangle \), \( \Gamma_{\text{m0}}^N \) the nonradiative decay rate due to energy transfer to the particle and \( K_{\text{m0}}^N \) the decay rate from intrinsic losses of the quantum emitter.\textsuperscript{35} The total decay rate \( \Gamma_{\text{m0}}^T \) is the sum of the three. The absorption takes the form \( \sigma_{\text{m0}}^{\text{abs local}} = 1/2 \sigma_{\text{m0}}^{\text{abs}} \epsilon / \mu |K_{\text{m0}}|^2 E_{\text{m0}} \cos(\theta) \), with \( \mu \) and \( \epsilon \) the permeability and permittivity of the medium, \( \sigma_{\text{m0}}^{\text{abs}} \) the absorption cross section for the concerned transition, and \( I_{\text{m0}} \) the local intensity as defined by the equality. \( \cos(\theta) \) accounts for the projection of the field in the absence of particle \( E_{\text{m0}} \) to the direction of the dipolar transition of interest. A possible polarization rotation due to the particle is included in \( K_{\text{m0}} \). The relaxation is considered to be fast enough for the population of the first excited level \( |1\rangle \) to be negligible. Under the weak excitation assumption so that stimulated emission can be neglected, the rate equations are

\[
\begin{align*}
\dot{N}_m &= -N_m \frac{\sigma_{\text{m0}}^{\text{abs local}}}{\hbar \omega_{\text{m0}}} + N_l \Gamma_{\text{m0}}^T. \\
\end{align*}
\]

\( N_m \) refers to the population of level \( |m\rangle \) and \( N_{\text{null}} \) the population of all levels of the quantum emitter, \( N_{\text{null}} - N_0 \) for weak excitation. The first term on the right hand side of the second equation describes the excitation of a quantum emitter from the ground level and the second term the total decay rate from the intermediate to the ground level at frequency \( \omega_{\text{m0}} \). In stationary regime, \( \partial/\partial t = 0 \). Since, \( \sigma_{\text{m0}}^{\text{local}} \propto |K_{\text{m0}}|^2 \), we find from the population equations that \( N_0 \propto \Gamma_{\text{m0}}^T / \Gamma_0^T \). The physics is clear: in the low intensity regime, the absorption increases linearly with the enhancement of the intensity \( |K_{\text{m0}}|^2 \) so that the population of the excited state increases also linearly. Conversely, the increased total decay rate decreases the population. When writing that the emitted power is proportional to \( \Gamma_{\text{m0}}^T N_r \), we find that the power is proportional to the quantum yield \( \eta_0 = \Gamma_{\text{m0}}^T / \Gamma_0^T \). The comparison of fluorescence signals with and without nanoparticle finally yields the equation

\[
\frac{P_{\text{out}}}{P_0} = |K_{\text{m0}}|^2 \frac{\eta_0}{\eta_0^0}.
\]

### 3. Upconversion: ESA

Limiting ourselves for simplicity to the simple scheme in Fig. 1(d), the rate equations for ESA, under weak excitation intensity and neglecting direct excitation to level \( |2\rangle \), are

\[
\begin{align*}
\dot{N}_0^e + N_1^e + N_2^e &= N_{\text{null}}, \\
\dot{N}_0^e &= -N_0^e \frac{\sigma_{01}^{\text{abs local}}}{\hbar \omega_{10}} + N_1^e \Gamma_{10}^e, \\
\dot{N}_1^e &= N_0^e \frac{\sigma_{01}^{\text{abs local}}}{\hbar \omega_{10}} - N_1^e \Gamma_{10}^e - N_2^e \Gamma_{21}^e, \\
\end{align*}
\]

Proceeding similarly as before, with \( N_{\text{null}} - N_0^e \gg N_1^e \gg N_2^e \) due to the weak excitation, and \( \Gamma_{01}^e = \Gamma_{12}^e \) for our energy levels and identical polarization dependence of both transitions, we obtain for the upconverted signal at \( \omega_{20} \).

\[
\frac{P_{\text{out}}}{P_0} = |K_{01}|^2 \frac{\Gamma_{10}^e \eta_{20}}{\Gamma_{10}^e \eta_{20}^0}.
\]

In general, \( \eta_{20} = \Gamma_{20}^e / (\Gamma_{20}^e + \Gamma_{21}^e) \), but in Sec. IV we considered \( \Gamma_{21}^e \) to be negligible for both ESA and NRET.

### 4. Upconversion: NRET

Under the same assumptions than for ESA and the NRET scheme in Fig. 1(e), we can write

\[
\begin{align*}
\dot{N}_0^N + y N_1^N + N_2^N &= y N_{\text{null}}, \\
\dot{N}_0^N + N_1^N &= N_{\text{null}}, \\
\dot{N}_0^N &= -N_0^N \frac{\sigma_{01}^{\text{abs local}}}{\hbar \omega_{01}} + N_1^N \Gamma_{01}^N, \\
\end{align*}
\]

\( N_0^N, N_1^N \) and \( N_{\text{null}} \) the population of the first excited level \( |2\rangle \) and \( |3\rangle \), respectively. The first term on the right hand side of the second equation describes the excitation of a quantum emitter from the ground level and the second term the total decay rate from the intermediate to the ground level at frequency \( \omega_{01} \).

\[
\frac{P_{\text{out}}}{P_0} = |K_{01}|^2 \frac{\eta_0^N}{\eta_0^N}.
\]
where necessary to avoid confusion, a further index at the upper left side, as, for example, in $^{y}N_{1}$, distinguish between the quantum systems $y$ and $x$, where $y$ emits the photon at $\omega_{\text{out}}$ and $x$ is at the origin of the energy transfer. We have followed Page et al. and assumed that the two quantum systems in fast equilibrium, with an equilibrium decay rate $\frac{\text{eq}}{10}$ common for the two levels $|1\rangle$ and the population relationship expressed by the fourth equality. There, $\gamma_{m}^{\text{m}}$ is the partition function for the level $m$ of $x$ and $\Delta E (=0$ in this paper) is the energy gap between the first excited level of $y$ and $x$. The efficiency of the nonradiative transfer to level $|2\rangle$ is proportional to the population of both $|1\rangle$ levels, with $\phi_{12}$ the proportionality constant. We assume that the particle affects the equilibrium decay rate in the same way as for a simple quantum emitter. Solving the equations and using the definition of the quantum yield as before, we obtain for the upconverted signal,

$$\frac{p_{\text{out}}}{p_{0}} = K_{01}\left(\frac{\text{eq}}{10} \frac{\eta_{210}}{\gamma_{210}} \frac{\eta_{20}}{\gamma_{20}}\right).$$

where, assuming the two quantum systems sufficiently close, of same polarization dependence and with identical frequency difference between the ground and the first excited level, we have used $K_{01} = K_{01}^{\text{m}}$. We have also neglected any change due to the particles in the energy transfer between the two quantum systems, otherwise a term of the form $\phi_{12}/\phi_{01}$ would appear.

**APPENDIX B: OTHER SCENARIOS**

Real upconversion systems can have complicated level schemes, and their exact configuration may significantly affect the emitted signal. We illustrate now for ESA the consequences of several changes on the energy level scheme of the quantum emitter.

Figure 7 focuses on changes on the decay path for quantum emitters excited to level $|2\rangle$. Such quantum emitters decay fast to an intermediate level $|2i\rangle$, from which it can decay to $|1i\rangle$ or $|0\rangle$—emitting a photon, transferring the energy nonradiatively to the particle or losing its energy due to the intrinsic losses [Fig. 7(a)]. The particular case $|1i\rangle = |1\rangle$ and $|2i\rangle = |2\rangle$ reduce to the case illustrated in Fig. 1. For our numerical examples, if not otherwise mentioned, $|1i\rangle = |1\rangle$ and the $|2i\rangle \rightarrow |1i\rangle$ transition energy is 1.9 times the value for the excitation. The resulting equation looks very similar to Eq. (4),

$$\frac{P_{\text{out}}}{P_{0}} = K_{01}^{14} \frac{\Gamma_{210}^{0}}{\gamma_{20}^{10}} \frac{\eta_{210}}{\gamma_{210}},$$

with the quantum yield of interest here taking the form

$$\eta_{210} = \frac{\Gamma_{210}^{R} + \eta_{\text{NR}}^{R} + \gamma_{210}^{10} + \Gamma_{21i}^{NR} + \gamma_{210}^{10} + \gamma_{21i}^{NR}}{\Gamma_{2i0} + \gamma_{2i0}^{10} + \gamma_{210}^{10} + \gamma_{210}^{10} + \gamma_{21i}^{NR} + \gamma_{210}^{10} + \gamma_{21i}^{NR}}.$$

Notice that intrinsic losses or the presence of the $|2i\rangle \rightarrow |1i\rangle$ always diminish the quantum yield term, but not significantly the ratio of the quantum yield in the presence and the absence of metallic particles. Similar considerations apply to the decay $1/\Gamma_{10}^{0}$.

Figure 7(b) concentrates on the influence of the strength of the decay path from level $|2i\rangle$ to $|1i\rangle$, with $k_{21i}^{NR} = k_{21i}^{R} = 0$ negligible for all transitions. At wavelengths around 1400 nm, slightly to the red of the dipolar resonance, the decay rate from the transition $|2i\rangle \rightarrow |1i\rangle$ is increased more strongly than the radiative decay rate of interest $\Gamma_{210}^{R}$, which negatively affects the upconverted signal. We notice that the effect is weaker for the wavelength of the maximum enhancement because not only $\Gamma_{21i}^{R}$ but also $\Gamma_{210}^{R}$ increases significantly, the latter due to the effect of a higher order resonances. Indeed, for an adequate value of $\omega_{21i}$ the increase in $\Gamma_{21i}^{R}$ can boost the quantum yield with respect to the value in the absence of particle; the enhancement of the upconverted signal is then larger than if the quantum emitter always decay directly to the ground state. The achieved improvement is moderate in our example [Fig. 7(c)].

To analyze the effect of the intrinsic losses from the $|2\rangle$ level, we set $\Gamma_{2i1}^{R} = 0$ and change $k_{2i0}^{R} / \Gamma_{2i0}^{R}$. For particles where such intrinsic losses are considerable, an increase in the radiative decay rate $\Gamma_{2i0}^{R}$ due the particle can lead to a considerable larger quantum yield and subsequent signal increase [Fig. 7(d)].

Figure 8 centers on changes on the decay path from the first excited state. We consider that a quantum emitter excited to level $|1\rangle$ decays fast and nonradiatively to $|k\rangle$ before either absorbing a second photon and being excited to $|2\rangle$ or decaying to the ground level. The resulting equation is again similar to Eq. (4),

$$\frac{P_{\text{out}}}{P_{0}} = K_{01}^{14} \frac{\Gamma_{1i0}^{R} \eta_{20}}{\gamma_{20}^{10} \gamma_{20}^{10}}.$$

Intrinsic losses have a similar effect as before, and for large values the presence of the particle can significantly enhance
the emission of upconverted signal [Fig. 8(d)] by increasing the term $\Gamma_0^T/(\Gamma_0^T + \Gamma_0^F) = (\Gamma_0^{NR} + \Gamma_0^{FS})/(\Gamma_0^{NR} + \Gamma_0^{FS} + \Gamma_0^{FS})$. Using a $\omega_{0R}$ smaller than the excitation illumination allows to decouple the maximum of the total decay rate $\Gamma_0^T$ and near-field enhancement $K_{0R}$, and thus to boost the achievable increase in the upconverted signal. The effect for 100 nm radius in Fig. 8(b) is relatively small because for the chosen conditions and the wavelengths around the maximum the total decay rate is not a strong function of $\omega_{0R}$. We observe a much larger effect for 10 nm radius, Fig. 8(c); non-negligible enhancement of the upconverted signal becomes then possible also for small particles, in contrast to Fig. 6(a).

FIG. 8. (Color online) ESA scheme, where the photon from $|1\rangle$ decay non-radiatively to an intermediate state before being excited by a second photon or decaying to the ground state. (b)–(d) Excitation wavelength dependence for silver sphere, radial orientation, 15 nm distance to the surface and the level scheme in (a). (b) Results for changing $\omega_{0R}/\omega_{0F}$, with $k_0^{NR}=k_0^{FS}=0$ and 100 nm radius. (c) equivalent to (b) but for 10 nm radius. (d) Results for changing $k_0^{NR}/k_0^{FS}$ for $\omega_{0R}=0.9\omega_{0F}, 100$ nm radius and $k_0^{NR}=0$.

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