Deuterium abundance in the most metal-poor damped Lyman alpha system: converging on $\Omega_{b,0}h^2$

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ABSTRACT
The most metal-poor damped Lyα system known to date, at $z_{abs} = 2.61843$ in the spectrum of the QSO Q0913+072, with an oxygen abundance of only $\sim 1/250$ of the solar value, shows six well-resolved D i Lyman series transitions in high-quality echelle spectra recently obtained with the European Southern Observatory (ESO) VLT. We deduce a value of the deuterium abundance $\log (D/H) = -4.56 \pm 0.04$ which is in good agreement with four out of the six most reliable previous determinations of this ratio in QSO absorbers. We find plausible reasons why in the other two cases the $1\sigma$ errors may have been underestimated by about a factor of two. The addition of this latest data point does not significantly change the mean value of the primordial abundance of deuterium, suggesting that we are now converging to a reliable measure of this quantity. We conclude that $\langle \log (D/H) \rangle = -4.55 \pm 0.03$ and $\Omega_{b,0}h^2(\text{BBN}) = 0.0213 \pm 0.0010$ (68 per cent confidence limits). Including the latter as a prior in the analysis of the Wilkinson Microwave Anisotropy Probe (WMAP) five-year data leads to a revised best-fitting value of the power-law index of primordial fluctuations $n_s = 0.956 \pm 0.013$ (1σ) and $n_s < 0.990$ with 99 per cent confidence. Considering together the constraints provided by WMAP 5, $(D/H)_{0p}$, baryon oscillations in the galaxy distribution, and distances to Type Ia supernovae, we arrive at the current best estimates $\Omega_{b,0}h^2 = 0.0224 \pm 0.0005$ and $n_s = 0.959 \pm 0.013$.

Key words: quasars: absorption lines – quasars: individual: Q0913+072 – cosmology: observations.

1 INTRODUCTION

The exquisite precision with which the temperature anisotropies of the cosmic microwave background (CMB) have been mapped on the sky has allowed the determination of cosmological parameters to better than 10 per cent (Dunkley et al. 2008). It is still important, however, to measure these parameters with alternative methods, partly as a consistency check on the standard cosmological model, but also because the CMB fluctuations generally constrain combinations of more than one parameter (e.g. Bridle et al. 2003). The contribution of baryons to the present-day critical density, $\Omega_{b,0}h^2$, where as usual $h = H_0/100\,\text{km s}^{-1}\,\text{Mpc}^{-1}$, is one such example: the value of $\Omega_{b,0}h^2$ which best fits the power spectrum of CMB fluctuations is tied to other parameters, such as the spectral index of primordial density perturbations, $n_s$, and the optical depth to reionization, $\tau$ (see, for example, Pettini 2006).

The quantity $\Omega_{b,0}h^2$ can also be deduced from the primordial abundances of the light elements whose nucleosynthesis is the result of physical processes that are entirely different from the acoustic oscillations of the photon–baryon fluid imprinted on the CMB, and that took place at much earlier times – only a few hundred seconds, rather than a few hundred thousand years, after the big bang. Among the light elements produced by primordial nucleosynthesis, deuterium is the one whose abundance by number relative to hydrogen, $(D/H)_{0p}$, depends most sensitively on $\Omega_{b,0}h^2$, and is thus the ‘baryometer’ of choice (Steigman 2007; Molaro 2008).

Reliable measures of $(D/H)_{0p}$ are difficult to obtain, however. The astrophysical environments which seem most appropriate are the hydrogen-rich clouds absorbing the light of background QSOs at high redshifts, but rare combinations of: (i) neutral hydrogen column density in the range $17 \lesssim \log [N(\text{H})/\text{cm}^{-2}] \lesssim 21$, (ii) low metallicity [M/H] corresponding to negligible astration of D, and (iii) most importantly, low internal velocity dispersion of the absorbing atoms, allowing the isotope shift of only $81.6\,\text{km s}^{-1}$ to be adequately resolved, are required for this observational test to succeed. Thus, while the potential of this method was appreciated more than 30 years ago (Adams 1976) and first realized with the advent of 8–10 m class telescopes in the 1990s (Tytler et al. 1995),
the number of trustworthy measurements of (D/H)$_p$ is still only five or six (O’Meara et al. 2006; Steigman 2007).

There are strong incentives to increase these meagre statistics. On the one hand, the mean $(D/H)_p = (2.82 \pm 0.26) \times 10^{-5}$ implies $\Omega_{D,H}^2 (BBN) = 0.0213 \pm 0.0013$ (O’Meara et al. 2006) which agrees, within the errors, with the value $\Omega_{D,H}^2 (CMB) = 0.02273 \pm 0.00062$ obtained by Dunkley et al. (2008) from the analysis of five years of observations with the Wilkinson Microwave Anisotropy Probe (WMAP 5). On the other hand, the standard deviation among the six measures of $(D/H)_p$ in high-redshift QSO absorbers exceeds the dispersion expected from the individual errors (leading to a high value of $\chi^2$ of the six measurements about the weighted mean). This is probably due to the considerable difficulties in accounting for the full measurement errors (random and systematic) of astronomical observations, but is nevertheless a source of concern, particularly when viewed in conjunction with the as yet poorly understood dispersion of D/H values in the Milky Way (Linsky et al. 2006).

Additional measurements of the D/H ratio at high redshift should, in principle at least, lead to a more precise estimate of $(D/H)_p$, as well as to a better assessment of the reasons for the scatter of the existing values. Such improvements are not only of interest in a cosmological context, but also relevant to Galactic chemical evolution models in which the degree of stration of D is an important diagnostic (e.g. Romano et al. 2006; Steigman, Romano & Tosi 2007). In this paper, we report observations of deuterium absorption in a seventh high-redshift absorber, a very metal poor damped Ly$\alpha$ system (DLA) at $z_{abs} = 2.61843$, and consider their implications for the determination of $(D/H)_p$, $\Omega_{D,H}h^2$, and other cosmological parameters.\footnote{Damped Ly$\alpha$ systems are a class of QSO absorbers defined by their high column densities of neutral hydrogen, $\log[N(H)/\text{cm}^{-2}] \geq 20.3$ [see Wolfe, Gawiser & Prochaska (2005), and Pontzen et al. (2008) for recent reviews of DLAs].}

2 OBSERVATIONS

The existence of a metal-poor DLA at $z_{abs} = 2.61843$ in the line of sight to the bright ($V = 17.1$), $z_{em} = 2.785$, QSO Q0913+072 has been known for some time (Pettini et al. 1997; Ledoux et al. 1998; Erni et al. 2006). More recently, it has been realized that DLA systems of low metallicity are also likely to have simple kinematics, possibly reflecting an underlying mass–metallicity relation of the host dark-matter haloes (Ledoux et al. 2006; Murphy et al. 2007; Pontzen et al. 2008; Prochaska et al. 2008). The most metal-poor DLAs are thus likely to be among the most promising candidates for follow-up high-resolution spectroscopy aimed at resolving the isotope shift in high-order lines of the Lyman series.

To this end, we targeted Q0913+072 with a concerted series of observations in 2007, using UVES (Dekker et al. 2000) on the ESO VLT2. The data were acquired in service mode; including a few spectra retrieved from the UVES data archive, the total exposure time devoted to this QSO was 77 550 s. De-}

Pettini et al. (2008) presented an analysis of the chemical composition and kinematics of this and other metal-poor DLAs, from consideration of metal absorption lines due to H, C, N, O, Al, Si, and Fe; we refer the interested reader to that paper for details. Of relevance to the present work are the following main results. With relative abundances $[C/H] = -2.75$ and $[Fe/H] = -2.80$, the $z_{abs} = 2.61843$ system in Q0913+072 is the most metal-poor DLA known.\footnote{With the usual definition, $[X/Z] = \log(X/Z)_\odot - \log(X/Z)_\odot$.} Its oxygen abundance, $[O/H] = -2.37$, is also among the lowest recorded in damped systems. The metal lines arising in the neutral gas have a very simple kinematic structure, consisting of two components at $z_{abs} = 2.61828$ and 2.61843 ($\Delta v = 12.4 \text{ km s}^{-1}$), with low internal velocity dispersions, $b = 3.7 \text{ km s}^{-1}$ and 5.4 km s$^{-1}$, respectively (where $b = \sqrt{2/\sigma}$ and $\sigma$ is the one-dimensional velocity dispersion of the absorbing atoms along the line of sight). The column density of neutral gas is distributed between the two components in approximately 3:7 proportion (see fig. 1 and table 2 of Pettini et al. 2008).

While these characteristics bode well for the possibility of resolving the D component of the Lyman series lines, they do not guarantee it. It is often the case that partially ionized gas at nearby velocities, with optical depths too low to be recognized in the metal lines, can blend with the H and D absorption due to the DLA itself, and prevent a reliable measurement of $N(D)$. Partially ionized gas does in fact appear to contribute to the C$\alpha$ absorption lines in this DLA, but seems to be confined to positive, rather than negative, velocities relative to $z_{abs} = 2.61843$. As can be seen from Fig. 1, this is indeed, somewhat fortuitously, the case.

3 HYDROGEN AND DEUTERIUM ABSORPTION IN THE $z_{abs} = 2.61843$ DLA SYSTEM

3.1 Deuterium

In Fig. 1 we have reproduced on a velocity scale relative to $z_{abs} = 2.61843$ the normalized profiles of absorption lines in the Lyman series of the DLA, from Ly$\alpha$ to Ly10. Ly11 is also visible in the Ly10 panel, while higher order lines are all blended with one another, constituting an ‘effective’ Lyman limit from $\lambda_0 = 917 \text{ Å}$. It is clear from the high-order transitions that there is H absorption at positive velocities relative to the $z_{abs} = 2.61843$ DLA, extending to $v \sim +200 \text{ km s}^{-1}$. On the blue side, however, there appear to be no additional components over those seen in the metal lines, and the D1 absorption is clearly resolved in Ly$\delta$ and Ly$\gamma$ through to Ly11, six transitions in total. (In Ly$\alpha$, Ly$\beta$ and Ly$\gamma$, which have the highest transition probabilities, H i and D i are intrinsically blended, whereas in Ly$\delta$ and Ly$\gamma$, presumably unrelated absorption in the Lyman forest is blended with the absorption due to the DLA.)

The availability of many D i transitions with a range of optical depths, from the saturated Ly$\beta$ to the optically thin Ly10 and Ly11, allows for a precise determination of the column density $N(D)$. To this end, we fitted the profiles of the Lyman lines where the D1 absorption is resolved with theoretical Voigt profiles generated by the VPFIT (version 8.02) software package.\footnote{VPFIT is available at http://www.ast.cam.ac.uk/~rfc/vpfit.html.} It uses $\chi^2$ minimization to deduce the values of redshift $z$, logarithmic column density $\log[N/(\text{cm}^{-2})]$ and Doppler parameter $b$ (km s$^{-1}$) that best reproduce the observed absorption line profiles, taking into account
Figure 1. Observed profiles (black histograms) and fitted Voigt profiles (continuous red lines) of absorption lines in the Lyman series of the $z_{\text{abs}} = 2.61843$ DLA in Q0913+072. The $y$-axes of the plots show relative intensity. The two vertical tick marks in each panel indicate the expected locations of the main absorption component of the DLA in, respectively, H I (at $v = 0$ km s$^{-1}$ in the plots) and D I (at $v = -81.6$ km s$^{-1}$). A second absorption component, centred at $v = -12.4$ km s$^{-1}$, is resolved in the metal lines associated with this DLA, but the two components are blended in the intrinsically broader H I and D I absorption. Additional H I absorption is seen at positive velocities relative to the DLA, but its column density is $\sim 100$ times lower than that of the DLA and therefore does not contribute to the observed D I absorption lines (see text).
the instrumental broadening function in its $\chi^2$ minimization and error evaluation. We used the compilation of laboratory wavelengths $\lambda_{lab}$ and $f$-values by Morton (2003). In Table 1 we have collected relevant details of the absorption model fitted to the observed line profiles in Fig. 1; the corresponding theoretical profiles generated by VPFIT are shown with continuous red lines in Fig. 1.

As mentioned in Section 2, the metal lines detected in this DLA consist of two components (Pettini et al. 2008), with the parameters listed in Table 1 for OI. The two components are not clearly distinguished in D I because: (i) absorption by the lighter D is intrinsically broader (see discussion below), and (ii) the S/N ratio of the spectrum is lower at the shorter wavelengths of the high-order Lyman lines (at $z_{abs} = 2.61843$ the wavelength region between Ly8 and the Lyman limit is redshifted to $\lambda_{abs} = 3438–3318 \, \AA$, approaching the cut-off by atmospheric ozone). Thus, in the first step of the fitting process, we fixed the redshifts of the two components to be the same as those determined from the metal lines while keeping the values of $b$ and $N(D)I$ as free parameters to be optimized by VPFIT. The best-fitting values of $b$ and $N(D)I$ thus reached are consistent with those deduced for O I and other metal lines. The relative proportions of atoms between the two components are similar in all species and the $b$-values are broader in D than in O, as expected. Recall that the velocity dispersion of an absorption line is the quadratic combination of macroscopic (turbulence) and microscopic (temperature related) terms, i.e. $b_{tot}^2 = b_{mac}^2 + b_{c}^2$, while the former is presumably the same for all elements, the latter has an inverse dependence on the square root of the mass, since $b_{c}^2 = 2kT/m$ (e.g. Strömgren 1948). The higher $b$-values of the two absorption components in D than O imply temperatures of a few thousand degrees.

The model parameters listed in Table 1 correspond to a best-fitting value for the column density of D I (sum of the two components) of

$$\log[N(D)I]/cm^{-2} = 15.78 \pm 0.02,$$

but we stress then this value does not depend on the details of the ‘cloud’ model adopted. To test its robustness, we rerun VPFIT without any assumptions about the distribution of velocities of the absorbers. Using as a starting point a single absorbing component with unspecified redshift and $b$-value, VPFIT returned a best-fitting value, $\log[N(D)I]/cm^{-2} = 15.79 \pm 0.02$, that is only 0.01 dex higher than that obtained with the parameters in Table 1 (although this second model results in a higher value of $\chi^2$ between computed and observed profiles). Any other adjustment to the details of the profile fits, such as varying the relative proportions of D I between the two components and their $b$-values or changing the parameters of nearby absorption in the Lyman forest, resulted in even smaller differences in the total value of $\log[N(D)I]$ returned by VPFIT.

As a final comment here, we point out that the VPFIT-generated line profiles shown in Fig. 1 include a number of other components to the red of $z_{abs} = 2.61843$, required to reproduce the saturated profiles of the H I Lyman lines which extend to $v \simeq 200 \, \text{km} \, \text{s}^{-1}$. The parameters of these extra absorptions are poorly constrained, but do not influence the determination of $\log[N(D)I]$ because they involve column densities of less than $\sim 1/100$ that of the DLA and thus do not contribute to the observed D I absorption.

### 3.1.1 Consistency check with the apparent optical depth method

Since the D I absorption lines we observe are resolved, we can deduce the column density directly from the measured residual intensity in each wavelength, or velocity, interval across the absorption lines (e.g. Hobbs 1974). The apparent optical depth at velocity $v$, $\tau_{abs}(v)$, is related to the observed intensity in the line, $I_{obs}(v)$, by

$$\tau_{abs}(v) = -\ln[I_{obs}(v)/I_0(v)],$$

where $I_0(v)$ is the intensity in the continuum. With the assumption of negligible smearing of the intrinsic line profile by the instrumental broadening function, we have:

$$\tau(v) \approx \tau_{abs}(v).$$

The optical depth $\tau(v)$ is in turn related to the column density of D I atoms in each velocity bin, $N(v)$ in units of $cm^{-2} (\text{km} \, \text{s}^{-1})^{-1}$, by the expression

$$N(v) = \frac{\tau(v) \times m_e c}{\pi e^2} = \frac{\tau(v)}{f_\lambda(\lambda)} \times 3.768 \times 10^{14},$$

where the symbols $f$, $\lambda$, $c$, $e$ and $m_e$ have their usual meaning.

As emphasized by Savage & Sembach (1991), the attraction of the apparent optical depth method lies in the fact that no assumption has to be made concerning the velocity distribution of the absorbers. Furthermore, this method provides a consistency check when two or more transitions arising from the same atomic energy level, but with different values of the product $\lambda f$, are analysed, as is the case here. The run of $N(v)$ with $v$ should be the same, within the errors in $I_{obs}(v)$, for all such lines.

For D I in Q0913+072, we can apply the apparent optical depth analysis to four unsaturated transitions, from Ly7 to Ly10; the other lines in the D I Lyman series being either partly blended or saturated (see Fig. 1). For each transition, we deduced a value of $N(D)I$ by summing equation (3) over the $n$ velocity bins which make up the absorption profile:

$$N_{TOT} = \sum_{i=1}^{n} N_i(v).$$

From the known error in the value of $I_{obs}(v)$ in each velocity bin, $\delta I_{obs}(v)$, we calculated the error $\delta N_{TOT}$:

$$\delta N_{TOT} = \sum_{i=1}^{n} \delta N_i(v)^2,$$

which is asymmetric about $N_{TOT}$ because of the non-linear nature of equation (1).

Fig. 2 shows the run of $N_i(v)$ across the four D I absorption lines, while values of $N_{TOT}$ and $\delta N_{TOT}$ are listed in Table 2. As can be seen from Fig. 2 and Table 2, the four D I absorption lines are in
good mutual agreement, and the standard deviation between the four independent measures of \( N(D) \) is \( 1 \sigma = 0.35 \times 10^{15} \) cm\(^{-2} \), or \( \sim 6 \) per cent of the mean. The weighted mean of the four values of \( N(D) \) returned by the apparent optical depth analysis is \( N(D) = (5.93^{+0.21}_{-0.16}) \times 10^{15} \) cm\(^{-2} \), where the uncertainties quoted are the errors on the weighted mean. On a logarithmic scale \( \log[N(D)/\text{cm}^{-2}] = 15.775 \pm 0.014 \), in very good agreement (as expected) with the value of \( \log[N(D)/\text{cm}^{-2}] = 15.78 \pm 0.02 \) returned by VPFIT, which we retain in the subsequent analysis.

### Table 2. Results of apparent optical depth analysis of D\( I \) lines.

| Transition | \( \lambda_{\text{lab}}^a \) (Å) | \( f^a \) | \( N_{\text{TOT}}(D) \) \((10^{15} \text{ cm}^{-2})\) |
|------------|-------------------------------|---------|---------------------------------|
| D\( I \)Ly7 | 925.9737                      | 0.003184| 5.64^{+0.43}_{-0.25}            |
| D\( I \)Ly8 | 922.899                       | 0.002216| 6.35^{+0.40}_{-0.29}            |
| D\( I \)Ly9 | 920.712                       | 0.001605| 6.08^{+0.37}_{-0.32}            |
| D\( I \)Ly10| 919.102                       | 0.001201| 5.61^{+0.41}_{-0.37}            |
| Weighted mean |                             |         | 5.93^{+0.21}_{-0.16}            |

\(^{a}\)Morton (2003).

#### 3.2 Hydrogen

Fig. 3 shows the region encompassing the damped Ly\( \alpha \) line. In principle, the column density of neutral hydrogen should be tightly constrained from the shape of the damping wings which extend over many hundreds of pixels (and are thus extremely well sampled by the data). In practice, the limiting factors are the uncertainty in the determination of the continuum level (to which the absorption is normalized) and the overlapping absorption from the narrower lines in the Ly\( \alpha \) forest. After numerous trials varying the continuum level and the weights given to different spectral intervals deemed to be free of overlapping absorption (see Kirkman et al. 2003 for a more extensive discussion of the problem), we converged on the best-fitting value:

\[
\log[N(H)/\text{cm}^{-2}] = 20.34 \pm 0.04;
\]

the corresponding theoretical damped profile is overplotted on the data in Fig. 3.

It is difficult to reliably estimate the systematic error which may be affecting this determination. While consistent with the above
estimate of \( \log N(H\text{I}) \) from Ly\( \alpha \), the higher order Lyman lines do not help to reduce the error further because they are all saturated and their equivalent widths include uncertain contributions from the lower column density components to the red of the DLA. In future, it may be possible to improve on the accuracy with which values \( N(H\text{I}) \) can be deduced from the analysis of damped profiles buried within the Ly\( \alpha \) forest by developing more sophisticated statistical methods to deal with the overlapping absorption, perhaps analogous to those used to subtract foreground Galactic emission from maps of the CMB. For the moment, we can perhaps obtain an indication of the magnitude of the systematic uncertainty in \( N(H\text{I}) \) by considering three previous estimates of this quantity, reported by different authors who used different spectrographs and telescopes, as follows: \( \log[ N(H\text{I})/\text{cm}^{-2}] = 20.36 \pm 0.08 \) (Pettini et al. 1997); 20.2 \pm 0.1 (Ledoux et al. 1998); 20.36 \pm 0.05 (Erni et al. 2006).

Of these, only the last one refers to a (small) subset of the data used here. From these results, it appears that our present estimate, \( \log[ N(H\text{I})/\text{cm}^{-2}] = 20.34 \pm 0.04 \), is unlikely to be in error by more than the stated margin.

From the values of \( N(D\text{I}) \) and \( N(H\text{I}) \) deduced in Sections 3.1 and 3.2, we arrive at the determination of the deuterium abundance in the \( z_{\text{abs}} = 2.61843 \) DLA system in line to Q0913+072 of:

\[
\log (D/H) = -4.56 \pm 0.04
\]

(where the errors have been combined in quadrature).

### 4 The Primordial Abundance of Deuterium

In Table 3 we have collected relevant measurements for all the high-redshift QSO absorption systems where the isotope shift has been resolved in absorption lines of the Lyman series. This prime sample of what are generally considered to be the most reliable measures of D/H at high \( z \) now consists of seven independent determinations. Other reports in the literature (e.g. Levshakov et al. 2002; Chrighton et al. 2004), while still interesting, refer to spectra of less straightforward interpretation because not all the D\( \text{I} \) components are resolved, so that the values of D/H deduced are more dependent on the precise description of the kinematics of the gas than is the case for the seven absorbers listed in Table 3 (see also the discussions of this point by Kirkman et al. 2003 and O'Meara et al. 2006).

All the measurements of D/H in Table 3 should be representative of the primordial abundance (D/H)\( _{\text{p}} \), because in all seven cases the gas has undergone little chemical enrichment, as evidenced by the low abundance of O (and other heavy elements), less than 1/10 of solar (see Column 5 of Table 3). For comparison, the total degree of astration of D over the lifetime of the Milky Way amounts to only \( \lesssim 20 \) per cent, if one accepts the possibility that in the local interstellar medium some of the deuterium may be depleted on to dust grains (Linsky et al. 2006). Theoretically, galactic chemical evolution models (e.g. Prantzos & Ishimaru 2001; Romano et al. 2006) show negligible reduction in D/H from the primordial value when the gas metallicities are as low as those of the seven QSO absorbers in Table 3, while observationally no trend is observed between D/H and O/H (Pettini 2006). Dust depletion of D is not expected to be an issue here, given the very low depletions of even the most refractory elements at these low levels of chemical enrichment (e.g. Akerman et al. 2005).

We arrive at an estimate of log (D/H)\( _{\text{p}} \) by averaging the individual measure of \( \log (D/H) \) in Table 3 to obtain the weighted mean

\[
\langle \log (D/H) \rangle = -4.55 \pm 0.02.
\]

However, the scatter of the points about this value is rather high for the quoted error bars assuming a Gaussian error model, giving \( \chi^2 = 19 \) which formally corresponds to a high probability that a further independent experiment would obtain a better fit to the data, \( P(\chi^2 > 19) < 0.01 \). This suggests that the errors on the individual measures of D/H may have been underestimated – a well-known and much discussed (e.g. Steigman

### Table 3. Prime sample of D/H measurements in QSO absorption line systems.

| QSO       | \( z_{\text{em}} \) | \( z_{\text{abs}} \) | \( \log N(H\text{I}) \) | [O/H]\(^a\)  | \( \log (D/H) \) | Ref.\(^b\) |
|-----------|----------------------|----------------------|-------------------------|-------------|----------------|--------|
| HS0105+1619 | 2.640                | 2.53600              | 19.42 \pm 0.01          | -1.70       | -4.60 \pm 0.04 | 1      |
| Q0913+072  | 2.785                | 2.61843              | 20.34 \pm 0.04          | -2.37       | -4.56 \pm 0.04 | 2, 3   |
| Q1009+299  | 2.640                | 2.50357              | 17.39 \pm 0.06          | < -0.67\(^c\) | -4.40 \pm 0.07 | 4      |
| Q1243+307  | 2.558                | 2.52566              | 19.73 \pm 0.04          | -2.76       | -4.62 \pm 0.05 | 5      |
| SDSS J155810.16−003120.0 | 2.823 | 2.70262 | 20.67 \pm 0.05 | -1.47 | -4.48 \pm 0.06 | 6 |
| Q1937−101  | 3.787                | 3.57220              | 17.86 \pm 0.02          | < -0.9      | -4.48 \pm 0.04 | 7      |
| Q2206−199  | 2.559                | 2.07624              | 20.43 \pm 0.04          | -2.04       | -4.78 \pm 0.09 | 2, 8   |

\(^a\)Relative to the solar value log (O/H)\( _{\odot} \) = 12 + 8.66 (Asplund, Grevesse & Sauval 2005).

\(^b\)References – (1) O’Meara et al. (2001), (2) Pettini et al. (2008), (3) This work, (4) Burles & Tytlle (1998b), (5) Kirkman et al. (2003), (6) O’Meara et al. (2006), (7) Burles & Tytlle (1998a), (8) Pettini & Bowen (2001).

\(^c\)This is a very conservative upper limit on the metallicity. Burles & Tytlle (1998b) estimate [Si/H] \( \simeq -2.5 \) and [C/H] \( \simeq -2.9 \) from photoionization modelling.
to \( \eta_{0.0} \) which measures the universal ratio of the densities of baryons and photons in units of \( 10^{-10} \):

\[
\eta_{0.0} = 10^{10} (n_b/n_\gamma) = 273.9 \Omega_{b,0} h^2. 
\]

The 3 per cent uncertainty in equation (7) is comparable to the uncertainties in the nuclear reaction rates used in big bang nucleosynthesis codes. The conversion from \( \eta_{0.0} \) to \( \Omega_{b,0} h^2 \) in equation (8) is accurate to about 0.1 per cent (Steigman 2006). From equations (6), (7) and (8), we find

\[
\Omega_{b,0} h^2 (BBN) = 0.0213 \pm 0.0009 \pm 0.0004, 
\]

where the error terms reflect the uncertainties in, respectively, \( \langle \sigma \rangle \) (equation 6) and the nuclear reaction rates (equation 7). Combining the two error terms in quadrature, we have

\[
\Omega_{b,0} h^2 (BBN) = 0.0213 \pm 0.0010. 
\]

The analysis by Dunkley et al. (2008) of five years of observations with the WMAP satellite concluded that, on the basis of the WMAP data alone,

\[
\Omega_{b,0} h^2 (CMB) = 0.02273 \pm 0.00062. 
\]

The two estimates of \( \Omega_{b,0} h^2 \) agree (just) within the errors; we also note that the uncertainty from BBN is now comparable to that from the CMB. Given that the best-fitting value of \( \Omega_{b,0} h^2 (CMB) \) is tied to those of other cosmological parameters, it is of interest to consider the effect of including the value of \( \Omega_{b,0} h^2 (BBN) \) as a prior in the analysis of the WMAP 5 data.

5 COMBINED CONSTRAINTS ON COSMOLOGICAL PARAMETERS FROM THE CMB AND \( \langle \text{D/H} \rangle \)

The five-year WMAP CMB temperature maps and large-scale polarization maps together provide tight constraints on several combinations of cosmological parameters (Dunkley et al. 2008; Hinshaw et al. 2008). In order to constrain individual parameters, however, it helps to apply external data that can break degeneracies. The baryon density, which affects the relative heights of the CMB acoustic peaks, is partly degenerate with the spectral index of primordial fluctuations, \( n_s \), since WMAP provides precision measurements of only two peaks in the temperature power spectrum. Increasing the value of \( n_s \) increases the height of the second peak, which can be compensated by a decrease in the baryon density. Hence, we can get a better constraint on the spectral index by combining the CMB data with an independent determination of \( \Omega_{b,0} h^2 \).

Among the alternative avenues to \( \Omega_{b,0} \) which have been considered, the primordial abundance of deuterium is the most accurate at present. The baryonic acoustic oscillations imprinted in the large-scale distribution of galaxies currently provide less stringent constraints on \( \Omega_{b,0} \) than either the CMB or \( \langle \text{D/H} \rangle \) and, in any case, really measure the combination of parameters \( \Omega_{b,0}/\Omega_{m,0} h \) (e.g. Blake et al. 2007). Measurements of other light elements created in big bang nucleosynthesis suffer from systematic uncertainties which are difficult to quantify (in the case of helium) or are poorly understood (for lithium), as discussed in recent reviews by Molaro (2008) and Steigman (2007) (see also Simha & Steigman 2008). In considering only deuterium in our joint analysis with the CMB, we make the implicit assumption that at present the primordial abundances of \(^1\text{H}\) and \(^7\text{Li}\) are difficult to reconcile with that of D because of astrophysical considerations (such as how to extrapolate from measured values in local astrophysical environments to the primordial abundances) and do not reflect an underlying departure from standard

\[
\Omega_{b,0} h^2 (CMB) = 0.02273 \pm 0.00062. 
\]
big bang nucleosynthesis. If the latter were the case, we would be unjustified in comparing the CMB fluctuations with only \((D/H)p\).

Parameter constraints from CMB data are usually encoded in a set of samples from the posterior distribution generated from the likelihood function by Markov Chain Monte Carlo methods. In combining the CMB data with the value reached here from \((D/H)p\), \(\Omega_{b,0} h^2(BBN) = 0.0213 \pm 0.0010\), we assume that the baryon density likelihood is an uncorrelated Gaussian. Since the constraint is only on one parameter, and consistent with the baryon density inferred from the CMB alone, we can use importance sampling to re-weight the parameter samples with the extra constraint (see Lewis & Bridle 2002 for details). For each sample in the original chain supplied by the WMAP team, we weight the sample by \(\exp[-(\Omega_{b,0} h^2 - 0.0213)^2/(2 \times 0.001^2)]\). Marginalized constraints for individual parameters can be calculated easily from the weighted chains; we use the ‘GetDist’ program provided with CosmoMC (Lewis & Bridle 2002) to do this.

### 5.1 Standard \(\Lambda\)CDM cosmological model

We assume the simplest flat \(\Lambda\) cold dark matter (\(\Lambda\)CDM) cosmological model, with a power-law purely adiabatic spectrum of linear primordial curvature perturbations with spectral index \(n_s\) and

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4 Available from http://lambda.gsfc.nasa.gov/product/map/dr3/parameters.cfm.
amplitude $A_s$ at $k = 0.002 \text{ Mpc}^{-1}$, dark matter density $\Omega_{c,0} h^2$, baryon density $\Omega_{b,0} h^2$, optical depth for sharp reionization $\tau$ and cosmological constant density relative to critical $\Omega_{\Lambda,0}$ (with a flat prior). Marginalized one-dimensional parameter constraints obtained in this way are shown in Fig. 5.

The combined constraint on the baryon density is $\Omega_{b,0} h^2 = 0.0223 \pm 0.0005$ where the error corresponds to the 68 per cent probability from the distribution shown in the top left panel of Fig. 5. For comparison, the value obtained by combining the WMAP 5 data with the distance measurements from Type Ia supernovae and the baryon acoustic oscillations in the large-scale distribution of galaxies is $\Omega_{b,0} h^2 = 0.02265 \pm 0.0006$ (Komatsu et al. 2008).

Since the (D/H)$_p$ measurement prefers values of the baryon density towards the lower end of the range allowed by the CMB, inclusion of this prior leads to a lower value of the spectral index: we obtain $n_s = 0.956 \pm 0.013$, and $n_s < 0.990$ at 99 per cent confidence (purely statistical errors). Thus, red spectral tilts are preferred and a Harrison–Zeldovich spectrum with $n_s = 1$ is ruled out in the simplest $\Lambda$CDM models. Other parameter constraints are almost unchanged, with only slight shifts in $\tau$, $\sigma_8$ and $H_0$ towards lower values. The combined goodness-of-fit parameter $\chi^2_{\text{min}}$ increases by about one on including the $\Omega_{b,0} h^2$(BBN) constraint, consistent with expectations for adding one independent parameter. Fig. 6 shows the combined constraints on $n_s$ and $\Omega_{b,0} h^2$ with and without the inclusion of the (D/H)$_p$ prior.

5.2 Constraints on a tensor component to primordial fluctuations

If the spectral index is less than one, some inflationary models predict an observable amplitude of primordial gravitational waves. Adding a parameter $r$ (with flat prior) to measure the ratio of the tensor and scalar power at $k = 0.002 \text{ Mpc}^{-1}$ is therefore well motivated (using the relation between the tensor and scalar tilts for the simplest inflation models; see Komatsu et al. 2008). A combination of WMAP 5 data and the (D/H)$_p$ constraint then gives $n_s < 1.00$, and a limit on the tensor amplitude $r < 0.26$, both at 95 per cent confidence. The constraints on these parameters are consistent with, and comparable to, those obtained by Komatsu et al. (2008) by considering WMAP data in conjunction with baryon oscillations and supernova distance measurements, but have completely different systematics. Considering all the constraints together – WMAP 5, (D/H)$_p$, Type Ia supernovae (Riess et al. 2004; Astier et al. 2006; Wood-Vasey et al. 2007) and baryon acoustic oscillations in the large-scale distribution of galaxies (Percival et al. 2007) – we arrive at the full joint probability distributions shown by the black continuous lines in Fig. 7. We find $r < 0.16$ at 95 per cent confidence and $n_s < 0.994$ at 99 per cent confidence. These limits strongly constrain possible models of the early universe, but are consistent with some of the simplest inflationary (and other) models. Joint marginalized constraints on the various parameters are as

Figure 7. Probability distributions of cosmological parameters deduced from the analysis of (i) WMAP 5 data alone (red dashed line), (ii) WMAP 5 + (D/H)$_p$ (blue dot-dashed line), (iii) adding to (ii) the constraints imposed by baryon acoustic oscillations in the large-scale distribution of galaxies and by the distances to Type Ia supernovae (black continuous line – see text for relevant references).
follows: \(\Omega_b h^2 = 0.0224 \pm 0.0005, \Omega_c h^2 = 0.1130 \pm 0.0034, \Omega_{k,0} = 0.723 \pm 0.015, h = 0.700 \pm 0.013, n_s = 0.959 \pm 0.013, \sigma_8 = 0.808 \pm 0.025\) and \(\tau = 0.818 \pm 0.016\) (1σ errors).

5.3 A closer look at the impact of the errors on D/H on the derivation of cosmological parameters

The results presented in Sections 5.1 and 5.2 assumed a Gaussian error on \(\Omega_b h^2\) derived from the dispersion of D/H measurements analysed with the bootstrap method. However, values for high-significance confidence limits are quite sensitive to the shape of the tails of the distribution and it is therefore worth assessing the robustness of our results to changes in the statistical model.

As discussed in Section 4, a Bayesian model that increases the error bars by some constant and marginalizes over the possible values of the constant gives an error estimate on \(\langle D/H \rangle_p\) which is comparable to that obtained with the bootstrap method. However, the tails of the distributions have quite different shapes. Fig. 8 shows the result of numerically evaluating the distribution of \(\Omega_b h^2\), assuming Gaussian errors on the \(D/H\) measurements, marginalizing over the additional error variance with a Jeffrey-like (i.e. inverse) prior on its amplitude, and including the 3 per cent error (also assumed to be Gaussian) in the relation between \(n_{10}\) and \(D/H_p\) (equation 7). The broad tails arise from marginalization over relatively large values of the added error variance, and fall off as a power law, rather than exponentially as in the bootstrap model. The result is not very sensitive to the inclusion or exclusion of the two most outlying data points in Fig. 4.

Using the marginalized results for additive additional error variance, the parameter constraints change somewhat from the values given in Sections 5.1 and 5.2. For example, combining the numerical baryon density likelihood with WMAP 5 data for tensor models, the 95 per cent limit on \(n_s\) changes from \(n_s < 1.00\) to \(< 1.01\) due to the tail of higher \(\Omega_b h^2\) values that are now allowed. The combined tightest constraints change to \(\Omega_b h^2 = 0.0226 \pm 0.0006\), \(n_s = 0.961 \pm 0.014\), with \(n_s \geq 1\) still just excluded at 99 per cent confidence and \(r < 0.17\) at 95 per cent confidence.

In both the Bayesian and bootstrap model, our results depend critically on the assumption that the quoted errors on the individual determinations of \(D/H\) in Table 3 (original and inflated) are statistically independent and Gaussian. The changes in the values of (or limits on) \(\Omega_b h^2, n_s, \) and \(r\) which we have just noted when changing the statistical model of the errors give an indication of the systematic error in the result due to the likelihood model, even when these assumptions are satisfied. In future, with a larger sample of measurements of \(D/H\) in QSO absorbers, it may be possible to test the assumptions that the errors are independent and Gaussian, and perhaps identify the origin of the excess scatter in the existing measurements. Such improvements would allow the primordial abundance of deuterium to fulfill its potential in constraining cosmological parameters. On a different note, the Planck satellite should independently measure the baryon density from the CMB alone with ~0.6 per cent accuracy in a few years, with measurements of several acoustic peaks breaking the degeneracy with \(n_s\).

6 SUMMARY AND CONCLUSIONS

The lowest metallicity damped Ly\(\alpha\) systems are good candidates for the measurement of the primordial abundance of deuterium, not only because the gas has suffered little astration, but also because they preferentially arise in gas clouds with low internal velocity dispersions, facilitating the resolution of the isotope shift of 82 km s\(^{-1}\). Furthermore, the high column densities involved give detectable D\(\alpha\) absorption in many lines of the Lyman series. The \(z_{\text{abs}} = 2.61843\) DLA in the spectrum of the bright QSO Q0913+072 is a good case in point – we have reported here high S/N detections of six D\(\alpha\) absorption lines from which we deduce log(D/H) = −4.56 ± 0.04. The main contribution to the error in log(D/H) is from the uncertainty in the column density of H\(\alpha\), rather than D\(\alpha\); it may be possible to reduce this further in future with more sophisticated modelling of the Lyman forest absorption that is superimposed on the wide, damped profile of the Ly\(\alpha\) line.

The value of D/H we deduce for this DLA is in good agreement with those of four out of the six QSO absorbers previously considered to constitute the most reliable set of such determinations. The other two differ from the mean of the whole sample by ~2\(\sigma\), and we have identified possible reasons why their errors may have been underestimated in the original reports. We propose that the determination of the primordial abundance of deuterium is converging towards the value (log(D/H)\(_p\)) = −4.55 ± 0.03, which can be considered reliable within the 68 per cent confidence limits. The corresponding \(\Omega_b h^2(BBN) = 0.0213 \pm 0.0010\) agrees within the errors with \(\Omega_b h^2(CMB) = 0.02273 \pm 0.00062\). Including the former as a prior in the analysis of the WMAP 5 data from which the latter is deduced results in a lower mean value of the power-law index of primordial fluctuations, from \(n_s = 0.963 \pm 0.015\) to 0.956 ± 0.013. The effects on other cosmological parameters deduced from the analysis of the CMB are more modest. Considering together the constraints available from WMAP 5, (D/H)\(_p\), baryon oscillations in the galaxy distribution, and distances to Type Ia supernovae, we arrive at the current best estimates \(\Omega_b h^2 = 0.0224 \pm 0.0005, n_s = 0.959 \pm 0.013\) (1σ errors) and \(r < 0.16\) (2σ limit) for the ratio of the tensor and scalar power at \(k = 0.002\) Mpc\(^{-1}\).

Despite the long integration time, the data presented here have not led to a significant change in the estimate of (D/H)\(_p\) compared with the last paper to report new observations (O’Meara et al. 2006). This is a good sign; together with the agreement between
\(\Omega_{\text{BBN}}\) and \(\Omega_{\text{CMB}}\), it suggests that we have reached a stage where the primordial abundance of deuterium and the cosmological density of baryons are sufficiently well determined quantities. There is now less urgency to increase further the number of D/H measurements in QSO absorbers, although a ‘prime’ sample of only seven data points clearly does not allow for complacency. In particular, an expanded sample of D/H measurements at high redshifts would improve the statistical model on which the errors on the derived cosmological parameters are based. The most metal-poor DLAs remain a fertile ground for studying early episodes of stellar nucleosynthesis (e.g. Pettini et al. 2008), and it is certainly worthwhile continuing to be aware of their potential for further refinements of (D/H).

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**APPENDIX A: UVES SPECTRUM OF Q0913+072**

For the interested reader, we provide in Table A1 the final reduced and co-added UVES spectrum of Q0913+072, as used in the work

**Table A1. UVES spectrum of Q0913+072.**

| Wavelength (Å) | Relative flux (arbitrary units) | 1σ error in relative flux |
|----------------|---------------------------------|--------------------------|
| 3.2999990E+03  | -4.8096318E+00                  | 1.9800955E+01            |
| 3.3000266E+03  | 7.2701191E+01                  | 2.1541672E+01            |
| 3.3000540E+03  | 8.8452042E+01                  | 1.9596445E+01            |
| 3.3000815E+03  | 6.0643616E+01                  | 1.8316616E+01            |
| 3.3001091E+03  | 5.9261909E+01                  | 2.0739399E+01            |
| 3.3001670E+03  | -8.5954037E+01                 | 2.0203918E+01            |
| 3.3001641E+03  | 6.8833572E+01                  | 1.9290850E+01            |
| 3.3001917E+03  | 9.1782742E+00                  | 1.893392E+00             |
| 3.3002192E+03  | -8.3213625E+00                 | 2.0355868E+01            |
| 3.3002468E+03  | 2.1003305E+01                  | 2.0274757E+01            |

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reported here and in Pettini et al. (2008). Relevant details are given in Section 2. The spectrum is available in its entirety in the online version of this paper. A portion is shown here for guidance regarding its form and content.

SUPPORTING INFORMATION

Additional Supporting Information may be found in the online version of this article.

Table A1. UVES spectrum of Q0913+072.

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