Studies of $WW$ and $WZ$ Production and Limits on Anomalous $WW\gamma$
and $WWZ$ Couplings

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Abstract

Evidence of anomalous $WW$ and $WZ$ production was sought in $p\bar{p}$ collisions at a center-of-mass energy of $\sqrt{s} = 1.8$ TeV. The final states $WW(WZ) \rightarrow \mu\nu\text{jet jet} + X$, $WZ \rightarrow \mu\nu\text{ee} + X$ and $WZ \rightarrow \text{eeee} + X$ were studied using a data sample corresponding to an integrated luminosity of approximately 90 pb$^{-1}$. No evidence of anomalous diboson production was found. Limits were set on anomalous $WW\gamma$ and $WWZ$ couplings and were combined with our previous results. The combined 95% confidence level anomalous coupling limits for $\Lambda = 2$ TeV are $-0.25 \leq \Delta\kappa \leq 0.39$ ($\lambda = 0$) and $-0.18 \leq \lambda \leq 0.19$ ($\Delta\kappa = 0$), assuming the $WW\gamma$ couplings are equal to the $WWZ$ couplings.

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Evidence of anomalous WW and WZ production was sought in pp collisions at a center-of-mass energy of $\sqrt{s} = 1.8$ TeV. The final states $WW(WZ) \rightarrow \mu\nu$ jet jet + X, $WZ \rightarrow \mu\nu eee + X$ and $WZ \rightarrow eee + X$ were studied using a data sample corresponding to an integrated luminosity of approximately 90 pb$^{-1}$. No evidence of anomalous diboson production was found. Limits were set on anomalous WWγ and WWZ couplings and were combined with our previous results. The combined 95% confidence level anomalous coupling limits for $\Lambda = 2$ TeV are $-0.25 \leq \Delta\kappa \leq 0.39$ ($\lambda = 0$) and $-0.18 \leq \lambda \leq 0.19$ ($\Delta\kappa = 0$), assuming the WWγ couplings are equal to the WWZ couplings.
I. INTRODUCTION

The gauge theory of the electroweak interactions contains a striking feature. Unlike the electrically neutral photon in quantum electrodynamics (QED), the weak vector bosons carry weak charge. Consequently, whereas in QED there are no photon-photon couplings, the weak vector bosons interact amongst themselves through the trilinear and quartic gauge boson vertices.

A formalism has been developed to describe the $WW\gamma$ and $WWZ$ vertices for the most general gauge boson self-interactions. The Lorentz invariant effective Lagrangian for the gauge boson self-interactions contains fourteen dimensionless couplings, seven each for $WW\gamma$ and $WWZ$:

$$\mathcal{L}_{WWV}/g_{WWV} = i g_1^V \left( W_{\mu\nu}^W V^{\nu} - W_{\nu}^V W_{\mu}^{\mu} \right) + i \kappa_V W_{\nu}^V W_{\mu}^{\mu\nu} + \frac{\lambda_V}{M_W^2} W_{\nu}^V W_{\mu}^{\mu\nu} + \frac{\gamma_1}{M_W^2} W_{\nu}^V W_{\mu}^{\mu\nu} + \frac{\gamma_2}{M_W^2} W_{\nu}^V W_{\mu}^{\mu\nu},$$

where $W^\mu$ denotes the $W^-$ field, $W_{\mu\nu} = \partial_{\nu} W^\mu - \partial_{\mu} W^\nu$, $V_{\mu\nu} = \partial_{\nu} V^\mu - \partial_{\mu} V^\nu$, $\tilde{V} = \frac{1}{2} \epsilon_{\mu\nu\rho\sigma} V^{\rho\sigma}$, and $(A \partial_{\mu} B) = A(\partial_{\mu} B) - (\partial_{\mu} A) B$. $V = \gamma$ and $Z$, and $M_W$ is the mass of the $W$ boson. The overall coupling parameters $g_{WWV}$ are $g_{WWW} = -e$ and $g_{WWZ} = e \cot \theta_w$, as in the standard model (SM), where $e$ and $\theta_w$ are the positron charge and the weak mixing angle. The couplings $\lambda_V$ and $\kappa_V$ conserve $C$ and $P$. The couplings $g_1^V$ are odd under $C$ and $g_2^V$ are odd under $C$ and $P$, and $\tilde{\kappa}_V$ and $\tilde{\lambda}_V$ are odd under $C$ and $P$. In the SM, all the couplings are zero at tree level with the exception of $g_1^V$ and $\kappa_V$ ($g_1^V = g_1^Z = \kappa_\gamma = \kappa_Z = 1$), and $\Delta \kappa_V$ and $\Delta g_2^V$ are defined as $\kappa_V - 1$ and $g_2^V - 1$, respectively. Electromagnetic gauge invariance restricts $g_1^V$, $g_1^Z$, and $g_2^Z$ to the SM values of $1, 0, 0$. The CP-violating $WW\gamma$ couplings $\lambda_\gamma$ and $\bar{\kappa}_\gamma$ have been tightly constrained by measurements of the neutron electric dipole moment to $|\bar{\kappa}_\gamma|, |\bar{\lambda}_\gamma| < 10^{-3}$.

With non-SM coupling parameters, the amplitudes for gauge boson pair production grow with energy, eventually violating tree-level unitarity. The unitarity violation is avoided by parameterizing the anomalous couplings as dipole form factors with a cutoff scale, $\Lambda$. Then the anomalous couplings take a form, for example,

$$\Delta \kappa(\hat{s}) = \frac{\Delta \kappa}{(1 + \hat{s}/\Lambda^2)^2},$$

where $\hat{s}$ is the invariant mass of the vector boson pair and $\Delta \kappa$ is the coupling value at the low energy limit. $\Lambda$ is physically interpreted as the mass scale where the new phenomenon which is responsible for the anomalous couplings would be directly observable.

Direct tests of the trilinear couplings are provided by $e^+e^-$ and $p\bar{p}$ colliders through production of gauge boson pairs, in particular by $e^+e^- \rightarrow W^+W^-$, $Z\gamma$, and $ZZ$ and by $p\bar{p} \rightarrow W^\pm\gamma$, $W^±W^-$, $W^±Z$, $Z\gamma$, and $ZZ$. The experiments seek to measure, or otherwise place limits on, trilinear couplings and to retain sensitivity to the appearance of new physical phenomena. The signature for anomalous trilinear couplings is an excess of gauge boson pairs, particularly for large values of the invariant mass of the gauge boson pair and for large values of gauge boson transverse momentum $p_T$.

Limits on these couplings are often obtained under the assumption that the $WW\gamma$ and $WWZ$ couplings are equal ($g_1^V = g_1^Z$, $\Delta \kappa_V = \Delta \kappa_Z$, and $\lambda_\gamma = \lambda_Z$). Another set of parameters, $\alpha_{\beta\phi}$, $\alpha_{W\phi}$, and $\alpha_W$, is similarly motivated by $SU(2)_L \times U(1)_Y$ gauge invariance. These couplings are linear combinations of $\lambda_V$, $\Delta \kappa_V$, and $\Delta g_2^V$ such that $\alpha_{\beta\phi} = \lambda_V - \Delta \kappa_V\cos^2 \theta_w$, $\alpha_{W\phi} = \Delta g_1^V\cos^2 \theta_w$, and $\alpha_W = \lambda_\gamma$ with the constraints that $\Delta \kappa_Z = -\Delta \kappa_\gamma\tan^2 \theta_w + \Delta g_2^Z$ and $\lambda_\gamma = \lambda_Z$. Adding the additional constraint that $\alpha_{\beta\phi} = \alpha_{W\phi}$ yields the HISZ relations used by the DØ and CDF collaborations.

The DØ collaboration has previously performed several searches for anomalous $WW\gamma$ and $WWZ$ couplings. Studies of $p\bar{p} \rightarrow W^+W^-\gamma$ have shown that the transverse energy spectrum of the photons agreed with that expected from SM production. Searches for an excess of $p\bar{p} \rightarrow W^+W^-\gamma$, where the $W$ bosons each decay to $e\nu$ ($\ell = e$ or $\mu$), yielded events which matched the SM prediction. Further, the $p_T$ spectrum of the charged leptons agreed with the prediction. Studies of the processes $p\bar{p} \rightarrow WW + X$ and $p\bar{p} \rightarrow WZ + X$, where one $W$ boson decayed to an electron or positron and the corresponding antineutrino or neutrino and the other vector boson decayed to a quark-antiquark pair manifested as jets, yielded no excess of events and a $W$ boson transverse energy spectrum which matched the expected background plus SM signal. Limits on anomalous $WW\gamma$ and $WWZ$ couplings were derived from each of these analyses. Several of these analyses were presented in detail in Ref. 12. The results of all of these analyses were combined using the method described in Ref. 12, to form our most restrictive limits on anomalous $WW\gamma$ and $WWZ$ couplings.

Limits on the $WW\gamma$ couplings have been set by the UA2 and CDF collaborations from the properties of $W + \gamma$ events and by the L3 Collaboration from the rate of single $W$ boson production at $\sqrt{s} = 172$ GeV. Both the $WWZ$ and $WW\gamma$ couplings have been studied by several experiments. CDF has searched for anomalous $WW$ and $WZ$ production and the four experiments at the LEP $e^+e^-$ collider have studied the properties of $WW$ events.

In this paper two new analyses resulting from a study
of $p\bar{p}$ collisions at a center-of-mass energy of $\sqrt{s} = 1.8$ TeV are presented. The collisions were recorded at DØ during the 1994–1995 and 1996 collider runs of the Fermilab Tevatron.

The first analysis is a search for $WZ$ production which provides a test of anomalous couplings unique among the gauge boson pair analyses. $WZ$ production is sensitive only to the $WWZ$ couplings, not the $WW\gamma$ couplings. In this analysis the collisions were searched for $WZ$ events where the $Z$ boson decayed to $ee$ and the $W$ boson decayed to either $e\nu$ or $\mu\nu$. The expected SM $WZ$ signal and the background were approximately equal in size and both were expected to be small. The number of events observed was compared with that expected from anomalous $WZ$ production in the presence of background to set upper limits on anomalous $WWZ$ couplings.

The second analysis is a search for anomalous $WW$ and $WZ$ ($WW/WZ$) production, similar to those of Refs. [10,11], using the decay signature $W \rightarrow \mu\nu, W/Z \rightarrow$ hadronic jets. Because SM $WW$ and $WZ$ production was swamped by backgrounds from other sources of $\mu\nu\bar{\mu}\bar{\nu}$ events, the analysis was sensitive only to anomalous vector boson pair production. The $p_T$ spectrum of the $\mu\nu$ system was compared to that expected from anomalous $WW$ and $WZ$ production plus the background, and limits on anomalous $WWZ$ and $WW\gamma$ couplings were produced.

The paper is arranged so that the subsequent two sections present common elements to the two analyses: the detector and particle identification. The fourth section presents elements common to the two analyses: the detector and particle identification. The fourth section contains the conclusion and summary of the results presented in this paper.

II. DETECTOR

The DØ detector consisted of four main systems: a non-magnetic inner tracking system, a liquid-argon uranium calorimeter, a muon spectrometer, and a trigger system. The detector is briefly described in this section. A detailed description of the detector is available in Ref. [12]. The tracker, calorimeter, and muon system are shown in Fig. 1.

A non-magnetic central tracking system, composed of central and forward drift chambers, provided directional information for charged particles and is used in this analysis to discriminate between electrons and photons, and in muon identification.

Particle energies were measured by a liquid-argon uranium sampling calorimeter that was divided into three cryostats. The central calorimeter (CC) covered pseudorapidity $|\eta| < 1.1$, and the end calorimeters (EC) covered $1.1 < |\eta| < 4.4$. The calorimeter was traversely segmented into projective towers with $\Delta \eta \times \Delta \phi = 0.1 \times 0.1$, where $\phi$ is the azimuthal angle. The third layer of the electromagnetic (EM) calorimeters, where the maximum energy deposition from EM showers was expected to occur, was segmented more finely into cells with $\Delta \eta \times \Delta \phi = 0.05 \times 0.05$. The scintillator-based intercryostat detectors (ICD’s), which improved the energy resolution for jets that straddled the central and end calorimeters, were inserted into the space between the cryostats. Thus, jet identification was performed in the whole calorimeter without any gap in pseudorapidity. Electron identification was performed for EM clusters with pseudorapidity $|\eta| \leq 2.5$; but the boundary between the CC and EC cryostats resulted in a gap spanning the region $1.1 \leq |\eta| \leq 1.5$.

The muon spectrometer consisted of solid-iron toroidal magnets and sets of proportional drift tubes (PDT’s). It provided identification of muons and determination of their trajectories and momenta. It consisted of three layers: a layer with four planes of PDT’s, located between the calorimeter and the toroid magnets; and two layers, each with three planes of PDT’s, located outside the toroid magnets. Figure 2 shows the geometric acceptance of the muon detector for the region $|\eta| \leq 1$ as determined from a Monte Carlo simulation of the detector. The muon momentum $p$ was determined from its deflection angle in the magnetic field of the toroid. The momentum resolution was limited by multiple scattering in the calorimeter and toroid, knowledge of the magnetic field integral, and the accuracy of the deflection angle measurement.

A multi-level, multi-detector trigger system [12] was used for selecting interesting events and recording them to tape. A coincidence between hits in two hodoscopes of scintillation counters (Level 0), centered around the beampipe, was required to register the presence of an inelastic collision. These counters also served as the luminosity monitor for the experiment. The Level 1 and Level 1.5 triggers were programmable hardware triggers which made decisions based on combinations of detector-specific algorithms. The Level 2 trigger was a farm of 48 VAX 4000/60 and 4000/90 computers which filtered the events based on reconstruction of the information available from the front-end electronics.

III. PARTICLE IDENTIFICATION

The analyses described in this paper rely on the detector’s ability to identify electrons, muons, hadronic jets,
and the undetected transverse energy due to neutrinos. A brief description of the particle identification criteria is presented in this section. A more detailed description of these particle identification criteria is available in Ref. [2].

A. Electron Identification

Electron candidates were identified using information from the calorimeters and tracking detectors. Electron candidates were formed from clusters, identified using a nearest-neighbor algorithm, with more than 90% of their energy in the EM layers of the calorimeter. The EM clusters had to fall within the CC ($|\eta| < 1.0$) or either EC $(1.5 < |\eta| < 2.5)$. Electrons had to be isolated, had to have a shower shape consistent with that from test beam measurements, and had to have either a track that closely matched the position of the shower centroid (“tight” selection criteria) or drift chamber hits consistent with the passage of a charged particle within an azimuthal road of width $\Delta \phi = 15$ (30) milliradians for CC (EC) EM clusters (“loose” selection criteria).

The efficiency for selecting electrons with the selection criteria described above was calculated using $Z \rightarrow ee$ decays. The efficiencies for each $\eta$ region and electron definition are shown in Table I. The energy resolution was $\sigma(E)/E = 14\% \sqrt{E/(\text{GeV})} \pm 0.3\% \pm 14\%/E(\text{GeV})$ for electrons in the CC and $\sigma(E)/E = 15.7\% \sqrt{E/(\text{GeV})} \pm 0.3\% \pm 29\%/E(\text{GeV})$ for electrons in the EC, where “⊕” indicates addition in quadrature.

B. Muon Identification

Muon candidates were tracks in the muon chambers which survived a number of reconstruction quality cuts. A muon was required to lie within the central region ($|\eta| < 1.0$). A muon had to pass through a region of the muon toroid with sufficient magnetic field $(Bdl > 2.0$ Tesla-meters). The energy deposited along the muon track in the calorimeter had to be at least that expected from a minimum-ionizing particle which on average deposits $\sim 1$ GeV. The impact parameter of the muon with respect to the interaction point had to be less than 20 cm. The muon track was refitted with the timing, $t_0$, of the muon track with respect to the collision as a floating parameter. It was required that $t_0$ be consistent with a muon originating from the interaction. A slightly different $t_0$ cut was used in the two analyses due to the different nature of the backgrounds. Lastly, the muon had to be separated by $\Delta R_{\mu} \equiv \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2} \geq 0.5$ from the nearest jet in the event. The muon reconstruction efficiency in the $WZ \rightarrow \mu\nu ee$ ($WW/WZ \rightarrow \mu\nu jj$) analysis for muons with $|\eta_{\mu}| < 1$ was $0.701 \pm 0.031 (0.680^{+0.041}_{-0.080})$ excluding losses due to the geometric acceptance of the muon detector. The muon momentum resolution was $\sigma(p)/p = 0.18(p - 2)/p^2 \pm 0.003$ ($p$ in GeV/c).

C. Jet Identification and Missing Energy

Jets were identified [2] as clusters of calorimeter towers within a cone centered on the highest $E_T$ tower. For the analyses described here, a cone size of $R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2} = 0.5$ was used. The energy deposited by the jet in the electromagnetic and hadronic calorimeters had to be consistent with that of an ordinary jet, thus suppressing the backgrounds from isolated noisy calorimeter cells and accelerator losses. These jet identification criteria have an efficiency of $0.96 \pm 0.01$ per jet. The jet energy resolution depended on the jet pseudorapidity and was approximately $\sigma(E)/E = 80%/\sqrt{E/(\text{GeV})}$.

The primary sources of missing transverse energy included neutrinos, which escaped undetected, and the energy imbalance due to the resolution of the calorimeter and muon system. Two calculations of missing transverse energy were made. The missing transverse energy which was calculated from the energy deposited in the calorimeter is referred to as $E_T^{cal}$. The missing energy which was calculated from the energy deposited in the calorimeter and was corrected for muons passing some loose quality cuts is referred to as $E_T$.

IV. SEARCH FOR WZ → TRILEPTONS

A search for $WZ \rightarrow \ell\ell\nu\nu$ production was performed in the $\ell\ell\nu\nu$ and $\mu\nu\ell\nu$ decay modes, taking advantage of the unusual signature consisting of three charged high-$E_T$ leptons and the missing transverse energy due to the high-$E_T$ neutrino.

A. Trigger and Data Sample

The Level 1 trigger used for this study required two EM calorimeter trigger towers ($\Delta \eta \times \Delta \phi = 0.2 \times 0.2$) with $E_T > 10$ GeV. The Level 2 trigger required two clusters of EM trigger towers which had $E_T > 20$ GeV and passed Level 2 isolation and shower shape cuts. The efficiency of the trigger was measured as a function of the reconstructed electron $E_T$ and found to be greater than 99% for a reconstructed $E_T > 25$ GeV. The integrated luminosity of the data sample was $92.3 \pm 5.0$ pb$^{-1}$. The luminosity determination is described in Ref. [21].
B. Event Selection Criteria

$WZ \to e\nu e\nu$ events were required to have two high-$E_T$ electrons consistent with a $Z$ boson decay, and a third electron and $E_T$ consistent with a $W$ boson decay. Specifically, at least one electron was required to satisfy the tight or loose selection criteria (as defined in Section III A). A tight electron and one of the other electrons were required to have $E_T > 25$ GeV and the third electron to have $E_T > 10$ GeV. It was required that $E_T^{\text{cal}} > 15$ GeV. The invariant mass of two of the electrons had to be within the range $81 < M_{e\nu} < 101$ GeV/c$^2$, as expected for the decay of a $Z$ boson. The transverse mass

$$M_T(e\nu) = \sqrt{2E_T^e E_T^{\text{cal}}(1 - \cos(\phi_e - \phi_{\nu}))}$$

calculated using the $E_T$ of the other electron and the $E_T^{\text{cal}}$ was required to be $M_T(e\nu) > 30$ GeV, as expected for the decay of a $W$ boson. These criteria were checked for all three combinations of electrons. One event was found which passed all the selection criteria. The parameters of this event are described in the appendix.

$WZ \to \mu\nu e\nu$ events were required to have two high-$E_T$ electrons as expected for a $Z$ boson decay, and a muon and $E_T$ consistent with a $W$ boson decay. Specifically, at least one electron was required to satisfy the tight selection criteria and another was required to satisfy the tight or loose selection criteria. Both electrons had to have $E_T > 25$ GeV. Instead of the 10 GeV third electron of the $e\nu e\nu$ search, a muon with $p_T > 15$ GeV/c was required. Finally, it was required that $E_T > 15$ GeV. No events passed these selection criteria.

C. Background Expected

The trilepton plus missing transverse energy signature demanded by the event selection has no known significant sources other than $WZ$ production and backgrounds due to objects misidentified as leptons.

In the $e\nu e\nu$ channel the largest background was expected to come from $Z + j$ events with $Z \rightarrow ee$ and where a jet mimicked an additional electron. This background was estimated using data. Events with two electron candidates and one or more jets were selected from the same data sample used in the event selection. The kinematic event selection criteria were applied treating each jet as the third electron. The probability for a jet to mimic a tight or loose electron was determined from a sample of multijet events and was parameterized by a linear function of jet $E_T$ for jets with $E_T$ less than $\sim 150$ GeV, as given in Table I. The background was then the number of $ee + j$ events times the probability of a jet mimicking the third (tight or loose) electron. This background was estimated to be $0.38 \pm 0.07$ (stat) $\pm 0.11$ (syst) events. The size of the statistical uncertainty was determined by the statistics of the $ee+$ jets sample. The systematic uncertainty was dominated by the 25% uncertainty in the probability for a jet to mimic a tight or loose electron. This latter uncertainty was due, in large part, to the uncertainty on the amount of direct photons in the multijet sample. A cross check based on a data sample of enriched with high EM jets which failed the electron selection criteria gave $0.42^{+0.41}_{-0.26}$ events for this background.

In the $\mu\nu e\nu$ channel there were two contributions to the background, one from events with two electrons and a jet which produced an isolated muon and one from events with an electron, a muon, and a jet which mimicked an electron. Data-based methods of calculating the background were used to estimate both of these contributions to the background.

To calculate the $ee+$ jet event background, events with two electrons and a central jet were selected (this was called the “fake” sample). Each event was required to pass all selection criteria except that the jet was only required to pass the muon fiducial and kinematic selection. The number of events was then multiplied by the probability of the jet producing an isolated muon, this probability having been determined using two methods. The probability (per jet) of finding an isolated muon in a sample of multijet events with $E_T(jet) > 15$ GeV was found to be $1.5 \times 10^{-5}$. The number of events expected from this background was $\leq 0.002$. On the other hand, a fraction of the $ee + j$ events contained heavy quark ($b/c$) jets. Assuming that all of the jets in the fake sample are heavy quark jets, a heavy-quark-enhanced fake rate was used to obtain an upper limit for this background. The probability of a jet mimicking a muon from a heavy quark ($b/c$) jet was found by requiring a muon (isolated or non-isolated) in the opposite hemisphere from the isolated muon in multijet events. This gave a heavy-quark-enhanced fake rate of $2.5 \times 10^{-4}$, resulting in an upper limit of $N_{bkg} = 0.022 \pm 0.004$ events. When setting limits on the cross section and coupling parameters, a smaller background estimate gives a more conservative limit. Therefore the lower estimate ($\leq 0.002$ events) was used in lieu of the larger (0.022 events).

The second background ($e\mu + j$-event) was calculated using events collected with a different trigger which required one EM object with $E_T > 20$ GeV and $E_T > 20$ GeV. Events were selected which had an isolated muon, one or more jets, and a tight or loose electron. All event selection cuts were applied with the exception of the trigger. The number of background events was then found by summing the $E_T$-dependent probability for a jet to have mimicked an electron for each event which passed the event selection criteria, accounting correctly for events which contained more than one jet and the difference in the integrated luminosities between the two triggers. The
F. Limits on Anomalous WWZ Couplings

The event generator and parameterized detector simulation were used, in a manner identical to that described above, to find the efficiency and expected number of events in the case of hypothetical anomalous WZ couplings. A grid in the $\lambda_Z-\Delta g_1^Z$ plane was used. Once the probability for observing one event was determined for each point in the grid, limits on the anomalous couplings were made. The limits were found by taking the logarithm of the likelihood and identifying the contour in $\lambda_Z - \Delta g_1^Z$ around the point of maximum of the logarithm of the likelihood ($L_{\text{max}}$) where $L = L_{\text{max}} - \delta$. To set a 95% C.L. limit in one dimension, the contour was evaluated at $\delta = 1.92$. To set a 95% C.L. limit in two dimensions (allowing two anomalous couplings to vary at the same time), the contour was evaluated at $\delta = 3.00$.

The value of the form factor scale $\Lambda$ was chosen such that the coupling limit was less than the unitarity limit. The one-dimensional 95% C.L. coupling limits and unitarity limits as a function of $\Lambda$ for each of the three coupling parameters are shown in Fig. 5.

This analysis was most sensitive to the parameters $\lambda_Z$ and $\Delta g_1^Z$. Setting $\Lambda = 1$ TeV, the one-dimensional 95% C.L. limits from the $e\nu e\nu$ and $\mu\nu e\nu$ channels are

$$|\Delta g_1^Z| < 1.63$$

$$|\lambda_Z| < 1.42$$

when all other parameters are held at their SM values. The two-dimensional 95% C.L. contour limits for $\Lambda = 1$ TeV are shown in Fig. 3 for the $e\nu e\nu$ and $\mu\nu e\nu$ data combined.

V. SEARCH FOR ANOMALOUS WW AND WZ PRODUCTION

The 1994–1995 data were searched for anomalous WW/WZ production in events with the signature: high-$p_T$ muon; large $E_T$; and at least two jets ($\mu\nu jj$).

A. Trigger and Data Sample

The Level 1 trigger consisted of a muon candidate in the central region and at least 5 GeV deposited in a hadronic trigger tower ($\Delta R \times \Delta \phi = 0.2 \times 0.2$). As the muon scintillation counters became available during the collider run they were added to the Level 1 trigger in such a way as to veto out-of-time muons, such as those that originated from cosmic rays.

The Level 2 trigger required a muon with $p_T > 10$ GeV/$c$, as determined by the muon pattern recognition algorithm taken from the reconstruction program. A
were selected. The muon was within the central region, $|\eta| < 2.5$. The jets were identified by a cone algorithm which summed $E_T$'s of calorimeter towers in cones of $R = 0.7$. The efficiency of the jet part of the Level 1 and Level 2 triggers was measured as a function of the reconstructed jet $E_T$ in three separate pseudorapidity bins by comparing the results of the single-muon trigger with the single-muon plus jet trigger for events which contained a single jet. Figure 3 shows the jet trigger efficiency as a function of jet $E_T$ for the pseudorapidity region $|\eta| < 1.0$. The jet trigger efficiency reached a plateau at jet $E_T$ of approximately 40 GeV. The efficiency was parameterized using an error function. The curve shown in Fig. 3 is the result of that fit. The results in the other two pseudorapidity regions were similar. For SM Monte Carlo events which passed all of the selection criteria, the efficiency of the jet part of the trigger was 0.927 ± 0.007. An alternate fit with a plateau at 100% increased this efficiency by 0.012 and that was taken as a systematic uncertainty. The efficiency of the muon component of the trigger was 0.707 ± 0.018. The integrated luminosity $20.3$ of the data sample was 80.7 ± 4.3 pb$^{-1}$.

**B. Event Selection Criteria**

The signature of the muon + jets channel consisted of an isolated high-$p_T$ muon from the $W$ boson decay and a minimum of two jets from a $W$ or $Z$ boson decay. We did not differentiate between the two processes $W \to jj$ and $Z \to jj$ due to the dijet mass resolution of the calorimeter. Single muon events with the following characteristics were selected. The muon was within the central region, which corresponded approximately to $|\eta| < 1$, and had transverse momentum $p_T^{\mu} \geq 20$ GeV/c. A $E_T$ of at least 20 GeV was required in each event. Demanding a transverse mass $M_T(\mu \nu) > 40$ GeV/c$^2$, where

$$M_T(\mu \nu) = \sqrt{2E_T^{\mu}E_T^{\nu}(1 - \cos(\phi_\mu - \phi_\nu))},$$

completed the kinematic selection defining the decay of a $W$ boson candidate. Next, the candidates had to contain at least two jets ($|\eta| < 2.5$) with $E_T \geq 20$ GeV. The invariant mass of the two highest $E_T$ jets had to be between 50 and 110 GeV/c$^2$ as expected for the decay of a $W$ or $Z$ boson. Figure 4 displays the distribution of the invariant mass of the two highest $E_T$ jets in the 372 events which remained in the sample after all selection criteria, except for the dijet mass selection, had been applied.

Application of the above cuts led to a final data sample of 224 events. The $p_T(\mu \nu)$ distribution for these events is shown in Fig. 4. The distribution indicates absence of events at $p_T(\mu \nu) > 150$ GeV/c. The $W$ boson candidate with the highest transverse energy had $p_T(\mu \nu) = 141$ GeV/c.

**C. Background Expected**

There were two major sources of background to the $WW/WZ \to \mu \nu jj$ production: $W + \geq 2$ jets with $W \to \mu \nu$; and QCD multijet events where one of the jets was accompanied by a muon which was misidentified as an isolated muon and where there was significant $E_T$. The latter background could have arisen from $b$-quark pair production, for instance. Contributions from other backgrounds such as: $WbW^{-}b^{-}$ production with subsequent decay to $W+\mu \nu$ followed by $W \to \mu \nu$; $WW/WZ$ production with $W \to \tau \nu$ followed by $\tau \to \mu \nu$, $ZX \to \tau \nu X$, where one of the muons was missing; and $ZX \to \tau \tau X$ with $\tau \to \mu \nu$, were small or negligible.

The QCD multijet background was estimated using a background enriched data sample. This technique was similar to that used in our previous analysis [36]. The probability for a jet with a muon to be misidentified as an isolated muon was determined from the ratio of the number of events containing an isolated muon, at least one jet, and $E_T$ less than 20 GeV to the number of events which contained a muon which failed the jet isolation requirement (but otherwise passed the muon identification cuts), two or more jets, and $E_T$ less than 20 GeV. This probability was 0.041 ± 0.007. Then the number of events which passed all of the selection criteria for the signal except for the muon-jet isolation requirement, again applied in reverse so as to form a sample complementary to the signal, was counted. This provided the sample of events for which misidentification of a non-isolated muon as an isolated muon would have created a false signal. There were 2567 such events. Thus the QCD multijet background was 105 ± 19 (stat) events. The QCD multijet background was also calculated for events which passed all the selection criteria for the signal except for the dijet invariant mass selection, which was applied in reverse.

This number was necessary for performing a background subtraction to the data in the out-of-mass cut region in order to calculate a normalization factor for the $W + \geq 2$ jets background. The QCD multijet background in the out-of-mass cut region was 55 ± 14 (stat) events.

The $W + \geq 2$ jets background was estimated using the VECBOS [17] event generator, with $Q^2 = (p_T^j)^2$, followed by parton fragmentation using the HERWIG [18] package and a detailed GEANT-based simulation of the detector. Normalization of the $W + \geq 2$ jets background was determined by comparing the number of events expected from the VECBOS estimate to the number of candidate events outside the dijet mass window, after the QCD multijet contribution had been subtracted. The contribution from this background was calculated to be 117 ± 24 (stat) events. A small component of the background, due to $Z + \geq 2$ jets with an unreconstructed muon which mimicked the $E_T$, was accounted for in this procedure because of the kinematic similarity to $W$ boson.
Among the other backgrounds, the only non-negligible contribution arose from $t\bar{t} \rightarrow W^+bW^-\bar{b}$ decays. This was estimated using a Monte Carlo sample produced similarly to that of the $W + \geq 2$ jets background sample. The $t\bar{t}$ background, calculated assuming a cross section of $5.5\pm1.8$ pb [39], amounted to $2.7\pm1.2$ events.

The total expected background was $224\pm31$ (stat) events. The number of observed events (224) was consistent with the background, and was much larger than the predicted SM WW/WZ signal (discussed in the next section). The systematic uncertainties in the QCD multijet background and the $W + \geq 2$ jets background were correlated because of the common uncertainty in the jet energy scale and because of the background subtraction carried out in the normalization procedure when the $W + \geq 2$ jets background was determined. As a cross check, the consistency between the background estimate and the number of observed events was verified for variations of the event selection criteria. The systematic uncertainties for the background estimation were: dijet mass window selection (13.4%); muon isolation (11.7%); jet energy scale (7.8%); missing transverse energy selection (7.2%); and $W$ boson transverse mass selection (4.3%). The total systematic uncertainty in the background was 46 events and the total uncertainty in the background was 56 events.

The contributions from all background sources are shown in Table IV. The estimates in the table for the components of the background include statistical uncertainties only. Figure 5 also displays the invariant mass of the two highest-$E_T$ jets from the expected background with all selection criteria, except for the dijet invariant mass selection, applied. The final distributions of the signal and the sum of backgrounds are plotted as a function of $p_T(W)$ in Fig. 6.

D. WW/WZ Signal Estimate

The efficiency for detecting $WW$ and $WZ$ events, for both SM and anomalous couplings, was determined using a leading-order event generator [40] and a parameterized simulation of the detector. The MRSD'- parton distributions [41] and a $k$-factor of 1.34 [2] were used in estimating the $WW/WZ$ cross section. In order to simulate the kinematics associated with higher-order production processes, the diboson decay products were boosted in the direction opposite to the hadronic recoil according to the $E_T$ distribution provided by PYTHIA [42] for SM $WW$ production. The efficiency was 2.5% lower when this boost was turned off, and half of this difference was taken as the fractional systematic uncertainty. The interaction points were selected around the center of the nominal collision point ($z=0$) from a Gaussian distribution with $\sigma = 30$ cm.

The muon fiducial acceptance was determined from a GEANT-based [43] detector model and is shown in Fig. 3. The jets from a high-$p_T$ $W$ or $Z$ boson decay may have been close enough to overlap and have poorly reconstructed energies, or they may have been completely merged into one jet. Therefore, the efficiencies of the jet selection and dijet mass selection depended on the boson’s $p_T$. SM $WW$ events, generated using PYTHIA Monte Carlo and the GEANT-based detector model, were used to determine this efficiency as a function of $p_T(\mu\nu)$. The results were incorporated into the parameterized detector simulation. Figure 5 shows the efficiency as a function of $p_T(\mu\nu)$ for events which passed the rest of the event selection criteria. The efficiency was low for low-$p_T$ $W$ boson events because of the jet $E_T$ threshold of 20 GeV. It peaked at 63% for $p_T(\mu\nu) = 200$ GeV/c and fell for higher $p_T$ because of jet merging. The uncertainty in the jet energy scale corrections led to a systematic uncertainty in the efficiency for $W$ and $Z$ boson identification of 3%.

The kinematic efficiencies for SM $WW$ and $WZ$ detection were $0.073\pm0.002$(stat) $\pm 0.003$(syst) and $0.067\pm0.002$(stat) $\pm 0.010$(syst), respectively, where the additional systematic uncertainty originates from differences between the acceptances calculated with the parameterized detector simulation and the acceptances calculated using PYTHIA and GEANT due to the jet reconstruction efficiency parameterization. Folding in the uncertainties due to the model of the jet trigger, the jet energy scale, and in the initial diboson boost, the systematic uncertainties in the kinematic efficiency amounted to 6.7% and 15.8% of the WW and WZ detection efficiency. Thus, the total efficiencies for SM WW and WZ production were $0.0351^{+0.0048}_{-0.0048}$ and $0.0322^{+0.0055}_{-0.0064}$, respectively. The efficiency was slightly higher for simulated WW and WZ production with anomalous $WW\gamma$ and/or $WZ$ couplings because the bosons originated at higher average $p_T$. For instance, for WW events produced with $\Lambda = 2.0$ TeV, the total efficiency was $0.038^{+0.004}_{-0.005}$ for the case $\lambda = 1.0$ and $\Delta\kappa = 0.0$, and $0.043^{+0.004}_{-0.006}$ for the case $\lambda = 2.0$ and $\Delta\kappa = 2.0$.

The predicted cross section [44] for SM $WW$ ($WZ$) production is 10.1 (2.6) pb. A 5% systematic uncertainty in this originates from the variation of the cross section depending on the set of parton distributions used in the event generation. The branching fractions [34] for $W \rightarrow \mu\nu$ and $W \rightarrow jets$ or $Z \rightarrow jets$ lead to overall branching fractions of $0.1412\pm0.0086$ and 0.0727$\pm0.0042$, respectively. Therefore, with an integrated luminosity of $80.7\pm4.3$ pb$^{-1}$, $4.04\pm0.68$ $WW$ events and 4.99$^{+0.10}_{-0.09}$ $WZ$ events were expected to have been detected if production is solely through SM processes.
E. Limits on Anomalous $WW\gamma$ and $WWZ$ Couplings

Since no excess of events in the high-$p_T(W)$ region was observed, significant deviations from the SM trilinear gauge couplings were excluded. Using the detection efficiencies for SM $WW$ and $WZ$ production and the background subtracted data, upper limits were set on the anomalous coupling parameters $\lambda$ and $\Delta\kappa$. This determination was made using a binned likelihood fit of the observed $p_T(W)$ spectrum to the prediction of the Monte Carlo signal plus the estimated background. Unequal width bins were used to evenly distribute the observed events, especially those in the high $p_T(W)$ region. In each $p_T$ bin for a given set of anomalous coupling parameters, the probability for the sum of the background estimate and Monte Carlo $WW/WZ$ prediction to fluctuate to the observed number of events was calculated. The uncertainties in the background estimations, efficiencies, integrated luminosity, and Monte Carlo signal modelling were convoluted into the likelihood function using Gaussian distributions.

The one-dimensional 95% C.L. limits on $\lambda$ and $\Delta\kappa$ are summarized in Table V for $\Lambda = 1$ TeV. The first two rows provide the coupling limits in the case of equal couplings for $\Lambda = 1.5$ TeV and 2.0 TeV. The two-dimensional bounds (corresponding to a logarithm of the likelihood function value 3.0 below the maximum value) for anomalous coupling parameters in the $\lambda - \Delta\kappa$ plane are shown in Fig. 11 for $\Lambda = 1.5$ TeV. Figure 12 also shows the bounds imposed by the unitary conditions as a larger ellipse.

VI. COMBINED RESULTS

The results of the two searches described in this paper have been combined with those of our previous publications using the procedure described in Ref. 12. The method was to perform a binned maximum likelihood fit of the number of events and their kinematic characteristics to the expected signals and backgrounds, taking care to account for correlated uncertainties among the data sets. The number of events and the expected background in the $WZ \rightarrow trileptons$ analysis of Section IV, and the $p_T(\mu\nu)$ spectrum as well as the expected background in the $WW/WZ$ analysis of Section V, were included into the multiple final state fit described in Ref. 13. The resulting limits on anomalous couplings represent the most restrictive available from our experiment.

Sets of limits were produced using the range of assumptions about the relations between the couplings as discussed in Section I. Table VII contains limits on $\lambda$, $\Delta\kappa$, and where applicable on $\Delta g^T_i$, for $\Lambda = 1.5$ and 2.0 TeV under each of the following assumptions: that the $WW\gamma$ couplings were equal to the $WWZ$ couplings; that the $WW\gamma$ couplings were related to the $WWZ$ couplings through the HISZ equations (with the additional constraint $\alpha_{B\phi} = \alpha_{W\phi}$); that the $WW\gamma$ couplings were at the SM values (producing limits on the $WWZ$ couplings); and that the $WWZ$ couplings were at the SM values (producing limits on the $WW\gamma$ couplings). Figure 11 shows the two-dimensional limit contours and one-dimensional limit points for $\lambda$ vs. $\Delta\kappa$ for these four relationships between the $WW\gamma$ and $WWZ$ couplings. Table VII contains limits on $\alpha_{B\phi}$, $\alpha_{W\phi}$, $\alpha_W$, and $\Delta g^T_0$ for $\Lambda = 1.5$ and 2.0 TeV. Figure 12 shows the two-dimensional limit contours and one-dimensional limit points for $\alpha_W$ vs. $\alpha_{B\phi}$ when $\alpha_{W\phi} = 0$ and for $\alpha_W$ vs. $\alpha_{W\phi}$ when $\alpha_{B\phi} = 0$. Note that the Fig. 11(a) limits on $\alpha_W$ vs. $\alpha_{B\phi}$ are equivalent to limits on $\lambda_0$ vs. $\Delta\kappa_0$ because $\Delta g^T_0$ is fixed to zero. Also, for purposes of comparison with LEP experiments, the central values and 68% C.L. limits on $\lambda_0$ and $\Delta\kappa_0$ were calculated under the HISZ relations (without the extra constraint $\alpha_{B\phi} = \alpha_{W\phi}$) for $\Lambda = 2.0$ TeV. They were $\lambda_0 = 0.00^{+0.10}_{-0.09}$ and $\Delta\kappa_0 = -0.08^{+0.34}_{-0.34}$.

VII. CONCLUSIONS

Using $p\bar{p}$ collisions at center-of-mass energy $\sqrt{s} = 1.8$ TeV detected with the DØ detector, two gauge boson pair production processes were studied and used to produce limits on anomalous trilinear gauge boson couplings.

A search for $WZ \rightarrow e\nu e\nu$ and $\mu\nu e\nu$ candidates yielded one candidate event where the expected signal from SM $WZ$ production was 0.25±0.02 events and the expected background was 0.50±0.17 events. The 95% C.L. upper limit on the cross section was 47 pb, consistent with, but rather larger than the expected SM cross section. Based on the one observed event, the detection efficiency, and the expected background, limits on anomalous $WWZ$ couplings were produced. The one-dimensional limits, at 95% C.L., are $|\Delta g^T_0| \leq 1.63$ ($\lambda_0 = 0$) and $|\lambda| \leq 1.42$ ($\Delta g^T_0 = 0$) for $\Lambda = 1.0$ TeV.

A search for anomalous $WW/WZ \rightarrow \mu\nu\mu\nu$ production was performed. The expected background of 224±56 events was much larger than the expected SM $WW$ and $WZ$ signal of 4.5±0.8 events. From the $p_T(\mu\nu)$ distribution of the 224 observed events, which had no significant deviation from the expected background plus SM signal, limits on anomalous $WW\gamma$ and $WWZ$ couplings were produced. Under the assumption that the $WW\gamma$ couplings equal the $WWZ$ couplings, the one-dimensional 95% C.L. limits were $-0.43 \leq \lambda \leq 0.44$ ($\Delta\kappa = 0$) and $-0.60 \leq \Delta\kappa \leq 0.74$ ($\lambda = 0$) for $\Lambda = 2.0$ TeV. Under the assumption that the $WW\gamma$ couplings are related to the $WWZ$ couplings via the HISZ equations, the one-dimensional 95% C.L. limits were $-0.42 \leq \lambda \leq 0.42$.
0.44 ($\Delta \kappa = 0$) and $-0.71 \leq \Delta \kappa \leq 0.96$ ($\lambda = 0$) for $\Lambda = 2.0$ TeV.

The results of the two searches described in this paper have been combined with those from our previous publications to produce our most restrictive limits on anomalous $WW\gamma$ and $WWZ$ couplings. Under the assumption that the $WW\gamma$ couplings equal the $WWZ$ couplings, the one-dimensional 95% C.L. limits were $-0.18 \leq \lambda \leq 0.19$ ($\Delta \kappa = 0$) and $-0.25 \leq \Delta \kappa \leq 0.39$ ($\lambda = 0$) for $\Lambda = 2.0$ TeV. Under the assumption that the $WW\gamma$ couplings are related to the $WWZ$ couplings via the HISZ equations, the one-dimensional 95% C.L. limits were $-0.18 \leq \lambda \leq 0.19$ ($\Delta \kappa = 0$) and $-0.29 \leq \Delta \kappa \leq 0.53$ ($\lambda = 0$) for $\Lambda = 2.0$ TeV. Limits on $\Delta \kappa$, $\lambda$, and $\Delta g^Z_1$ were determined for the $WW\gamma$ couplings assuming the $WWZ$ couplings are at the SM value, and for the $WWZ$ couplings assuming that the $WW\gamma$ couplings are at the SM value. Finally, limits on the $\alpha\beta_\phi$, $\alpha W_\phi$, and $\alpha W_\pi$ anomalous couplings were produced.

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VIII. APPENDIX: PARAMETERS OF THE $WZ$ CANDIDATE EVENT

Given the expected signal to background ratio of approximately one to two in the channel $WZ \rightarrow e\nu e\nu$, there is no certainty that the candidate event is actually due to $WZ$ production. But due to the event’s striking signature it is described in detail in this appendix.

The candidate event contains three high-$E_T$ electron candidates and large missing transverse energy (46.2 GeV). The event contains no other high-$p_T$ objects (jets or muons). The properties of the candidate electrons are summarized in Table VIII. The missing transverse energy and the various mass combinations of the electrons with the missing transverse energy are listed in Table IX. The invariant mass of electron candidates 1 and 3 is 93.6 GeV/$c^2$, and the transverse mass formed using electron candidate 2 and the missing transverse energy is 74.7 GeV/$c^2$.

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$$\Lambda = \left( \frac{4.33}{\lambda_Z^2 + \frac{M_W^2}{2M_Z^2} \Delta g_1^2} \right)^{\frac{1}{2}}$$

with $\Lambda$ given in TeV.

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TABLE I. Measured efficiencies for electron identification in the CC and two EC’s. See text for definitions of tight and loose.

| Electron Type | Efficiency (CC) % | Efficiency (EC) % |
|---------------|------------------|------------------|
| Loose         | 88.6 ± 0.3       | 88.4 ± 0.5       |
| Tight         | 73.4 ± 0.5       | 67.2 ± 0.3       |

TABLE II. Jet misidentification probabilities for tight and loose electrons. The probability is a linear function of $E_T$ (GeV), $a_0 + a_1 \times E_T$ (GeV). Uncertainties given in this table are statistical only. A systematic uncertainty of 25% was assigned to each fake probability.

| Electron Type | $a_0 \times 10^3$ | $a_1 \times 10^3$ | $a_0 \times 10^2$ | $a_1 \times 10^2$ |
|---------------|-------------------|-------------------|-------------------|-------------------|
| Loose         | 0.08 ± 0.29       | 2.06 ± 0.70       | 1.5 ± 1.0         | 6.31 ± 0.27       |
| Tight         | -0.17 ± 0.20      | 1.43 ± 0.51       | 0.53 ± 0.86       | 5.1 ± 2.3         |

TABLE III. Summary of the WZ → $llll$ results. $L$ is the integrated luminosity, $\epsilon$ is the overall detection efficiency, $Br$ is the branching ratio, $N_{obs}$ is the number of events observed, $N_{bg}$ is the number of background events, and $N_{SM}$ is the predicted number of SM events.

| Sample                  | Number of Events |
|-------------------------|------------------|
| QCD multi-jet background| 165±19 (stat)    |
| W + ≥ 2 jets background | 117±24 (stat)    |
| tt background           | 2.7±1.2 (stat)   |
| Total background        | 224±31 (stat + syst) |
| SM prediction           | 4.5±0.8 (stat + syst) |
| Observed data sample    | 224              |

TABLE IV. Comparison of signal (data) and backgrounds for the mode $WW/WZ \rightarrow \mu

TABLE V. Axis limits (one-dimensional) at the 95% C.L. with two assumptions for the relation between the $WW\gamma$ and $WWZ$ couplings ($WW\gamma = WWZ$ and HISZ) and for two different values of $\Lambda$ in the mode $WW/WZ \rightarrow \mu jj$.

| Coupling | $\Lambda = 1.5$ TeV | $\Lambda = 2.0$ TeV |
|----------|----------------------|----------------------|
| $\lambda_\gamma = \lambda_\gamma$ | $-0.45$, $0.46$ | $-0.43$, $0.44$ |
| $\Delta \kappa_1 = \Delta \kappa_2$ | $-0.62$, $0.78$ | $-0.60$, $0.74$ |
| $\lambda_\gamma = \lambda_\gamma$ (HISZ) | $-0.44$, $0.46$ | $-0.42$, $0.44$ |
| $\Delta \kappa_1$ (HISZ) | $-0.75$, $0.99$ | $-0.71$, $0.96$ |

TABLE VI. One-dimensional limits at 95% C.L. from a simultaneous fit to the DØ $WW\gamma$, $WWWZ \rightarrow e\nu ee\mu\nu$ data samples. The HISZ results included the additional constraint $\alpha_{B\phi} = \alpha_{W\phi}$.

| Coupling | $\Lambda = 1.5$ TeV | $\Lambda = 2.0$ TeV |
|----------|----------------------|----------------------|
| $\alpha_{B\phi}$ (SM $WW\gamma$) | $-0.20$, $0.20$ | $-0.18$, $0.19$ |
| $\alpha_{W\phi}$ (SM $WW\gamma$) | $-0.27$, $0.42$ | $-0.25$, $0.39$ |
| $\Delta \kappa_1$ (SM $WW\gamma$) | $-0.31$, $0.56$ | $-0.29$, $0.53$ |
| $\lambda_\gamma$ (SM $WWZ$) | $-0.26$, $0.29$ | $-0.24$, $0.27$ |
| $\Delta \kappa_1$ (SM $WWZ$) (HISZ) | $-0.37$, $0.55$ | $-0.34$, $0.51$ |
| $\Delta \kappa_1$ (SM $WWZ$) | $-0.39$, $0.62$ | $-0.37$, $0.57$ |
| $\lambda_\gamma$ (SM $WWZ$) (HISZ) | $-0.27$, $0.25$ | $-0.25$, $0.24$ |
| $\Delta \kappa_1$ (SM $WWZ$) | $-0.57$, $0.74$ | $-0.54$, $0.69$ |

TABLE VII. One-dimensional limits at 95% C.L. on $\alpha$ parameters from a simultaneous fit to the DØ $WW\gamma$, $WWWZ \rightarrow e\nu jj$, $WW/WZ \rightarrow \mu\nu jj$, and $WW \rightarrow \mu\nu jj$ data samples.

| Coupling | $\Lambda = 1.5$ TeV | $\Lambda = 2.0$ TeV |
|----------|----------------------|----------------------|
| $\alpha_{B\phi}$ | $-0.73$, $0.59$ | $-0.67$, $0.56$ |
| $\alpha_{W\phi}$ | $-0.19$, $0.38$ | $-0.18$, $0.36$ |
| $\Delta \kappa_1$ (SM $WW\gamma$) | $-0.20$, $0.20$ | $-0.18$, $0.19$ |
| $\Delta \kappa_1$ (SM $WWZ$) | $-0.25$, $0.49$ | $-0.23$, $0.47$ |

TABLE VIII. Kinematic properties of the $WZ \rightarrow e\nu ee$ candidate event (Run 89912, Event 23020).
Mass Combination Information

\begin{align*}
M_{e_1,e_2} &= 111.8 \text{ GeV/}c^2 \\
M_{e_1,e_3} &= 93.6 \text{ GeV/}c^2 \\
\not{E}_T &= 46.2 \text{ GeV} \\
M_T(e_1,\not{E}_T) &= 73.0, 74.7, 82.6 \text{ GeV/}c^2 \text{ for } e_1, \ e_2, \ e_3 \text{ respectively} \\
\not{p}_T(e_1,e_3) &= 58.8 \text{ GeV/}c \\
\not{p}_T(e_2,\not{E}_T) &= 63.0 \text{ GeV/}c \\
\phi(\not{E}_T) &= 1.29 \\
\phi(e_1,e_3) &= -1.02 \\
\phi(e_2,\not{E}_T) &= 2.22
\end{align*}

TABLE IX. Mass combination information for e\nu ee candidate event. \(M_{e_i,e_j}\) is the invariant mass of electron \(i\) and electron \(j\). \(M_{e_1,e_2,e_3}\) is the three-body mass of electron 1, electron 2, and electron 3. \(M_T\) is the transverse mass and \(p_T\) is the transverse momentum.

FIG. 1. Isometric view of the DØ detector. Also shown are the calorimeter support platform, the Tevatron beampipe centered within the calorimeter, and the Main Ring beampipe which penetrated the muon system and calorimeter above the detector center.

FIG. 2. The geometrical acceptance of the muon detector within the region \(|\eta| \leq 1\). \(\phi = \frac{2\pi}{3}\) is the downward (\(\hat{y}\)) direction where the calorimeter support platform breaks into the muon system three-layer geometry.
FIG. 3. One-dimensional 95% C.L. (solid) and unitarity limits (dashed) vs. $\Lambda$ for the $W W Z$ coupling parameters $\lambda_Z$, $\Delta \kappa_Z$, and $\Delta g_1^Z$.

FIG. 4. Correlated limits on $\Delta g_1^Z$ and $\lambda_Z$ for $\Lambda = 1$ TeV obtained from a fit to the cross section using the 1994–1996 data for the $\mu ee$ and $e ee$ channels combined. The inner solid line is the two-dimensional 95% C.L. limit and the outer solid line is the unitarity limit.

FIG. 5. Jet trigger efficiency in pseudorapidity region $|\eta| < 1.0$. The curve is the result of an error function fit to the efficiency.

FIG. 6. Comparison of invariant mass of the two highest $E_T$ jets for the data (histogram) and the estimated total background (points with uncertainties) for the $WW/WZ \rightarrow \mu \nu jj$ channel. The uncertainties shown are statistical only.
FIG. 7. Comparison of the $p_T(W)$ distributions of signal (histogram) and estimated total background (× with statistical uncertainties) for $WW/WZ \rightarrow \mu\nu jj$. They are consistent with each other indicating the presence of no significant anomalous gauge couplings.

FIG. 8. The efficiency of the dijet reconstruction and selection as a function of $p_T(\mu\nu)$ in the $WW/WZ \rightarrow \mu\nu jj$ analysis. The uncertainties shown are statistical only.

FIG. 9. Contour plot of allowed region in the $\lambda - \Delta\kappa$ space for $WW/WZ \rightarrow \mu\nu jj$ at 95% C.L. for $\Lambda = 1.5$ TeV. The outer ellipse shows the bounds imposed by the unitary relations on $\lambda$ and $\Delta\kappa$. The uncertainties shown are statistical only.
FIG. 10. Contour limits on anomalous couplings from a simultaneous fit to the DØ $W\gamma$, $WW \rightarrow$ dilepton, $WW/WZ \rightarrow e\nu jj$, $WW/WZ \rightarrow \mu\nu jj$, and $WZ \rightarrow$ trilepton final states for $\Lambda = 1.5$ TeV: (a) $\Delta \kappa \equiv \Delta \kappa_\gamma = \Delta \kappa_Z, \lambda \equiv \lambda_\gamma = \lambda_Z$; (b) HISZ relations; (c) SM $WW\gamma$ couplings; and (d) SM $WWZ$ couplings. (a), (c), and (d) assume that $\Delta g_3^2 = 0$. The solid circles correspond to 95% C.L. one-degree of freedom exclusion limits. The inner and outer curves are the 95% C.L. two-degree of freedom exclusion contour and the constraint from the unitarity condition, respectively. In (d), the unitarity contour is located outside of the boundary of the plot. The HISZ results include the additional constraint $\alpha_B = \alpha_W$.

FIG. 11. Contour limits on anomalous couplings from a simultaneous fit to the DØ $W\gamma$, $WW \rightarrow$ dilepton, $WW/WZ \rightarrow e\nu jj$, $WW/WZ \rightarrow \mu\nu jj$, and $WZ \rightarrow$ trilepton final states for $\Lambda = 1.5$ TeV: (a) $\alpha_W$ vs. $\alpha_B$ when $\alpha_W = 0$; and (b) $\alpha_W$ vs. $\alpha_W$ when $\alpha_B = 0$. The solid circles correspond to 95% C.L. one-degree of freedom exclusion limits. The inner and outer curves are the 95% C.L. two-degree of freedom exclusion contour and the constraint from the unitarity condition, respectively.