Rapid destruction of planetary debris around WDs through wind erosion

Mor Rozner,1* Dimitri Veras2,3† Hagai B. Perets1
1 Physics department, Technion - Israel Institute of Technology, Haifa, 320004, Israel
2 Centre for Exoplanets and Habitability, University of Warwick, Coventry CV4 7AL, UK
3 Department of Physics, University of Warwick, Coventry CV4 7AL, UK

ABSTRACT
The discovery of numerous debris disks around white dwarfs (WDs), gave rise to extensive study of such disks and their role in polluting WDs, but the formation and evolution of these disks is not yet well understood. Here we study the role of wind erosion in the evolution of solids in WD debris disks. Wind erosion is a destructive process that plays a key role in shaping the properties and size-distribution of planetesimals, boulders and pebbles in gaseous protoplanetary disks. Our analysis of wind erosion in WD debris disks shows it can also play an important role in these environments. We study the effects of wind erosion under different conditions of the disk, and its erosive effect on planetesimals and boulders of different sizes. We find that solid bodies smaller than ~ 5km will be eroded within the short disk lifetime. We compare the role of wind erosion in respect to other destructive processes such as collisional fragmentation and thermal ablation. We find that wind erosion is the dominant destructive process for objects with radius \( \leq 10^3 \text{cm} \) and at distances \( \leq 0.6R_* \) from the WD. Thereby, wind erosion constitutes the main destructive pathway linking fragmentational collisions operating on large objects with sublimation of the smallest objects and Poynting-Robertson drag, which leads to the accretion of the smallest particles onto the photosphere of WDs, and the production of polluted WDs.

Key words: stars: white dwarfs – planets and satellites: formation – planets and satellites: dynamical evolution and stability – minor planets, asteroids: general – planets and satellites: physical evolution

1 INTRODUCTION
White dwarfs (WDs) are the final evolutionary stage of the vast majority of all stars. Metal-polluted WDs, which represent 25 – 50% of the whole WD population (Zuckerman et al. 2010; Koester et al. 2014), constitute an observational signature of the accretion of heavy elements. A few per cent of the WDs are surrounded by planetary debris disks (Manser et al. 2020), and over sixty WD disks have already been discovered (Zuckerman et al. 2010; Farihi 2016). Most of the observed disks are dusty, although about twenty disks with gaseous components were discovered as well (Dennihy et al. 2020; Melis et al. 2020; Gentile Fusillo et al. 2020).

The quickly growing population of these disks motivates theore•

tical explorations of their structure and evolution, which can reveal both how they are formed (Veras et al. 2014, 2015; Malamud & Perets 2020a,b) and how they accrete onto WDs photospheres, creating observable metal pollution (Jura & Young 2014; Hollands et al. 2018; Harrison et al. 2018; Doyle et al. 2019; Swan et al. 2019; Bonsor et al. 2020). An interesting observed feature of WD disks is that nearly all the disks are now thought to showcase flux variability on timescales of weeks to decades (Farihi et al. 2018; Xu et al. 2018; Swan et al. 2020).

The abundance of objects with different sizes in WD disks – from grain size to minor planets, reveals rich and interesting dynamics (see a detailed review of post-main sequence evolution in Veras 2016), which includes many physical processes, among them are replenishment and accretion. Frequent collisions in WD disks (Jura 2008; Metzger et al. 2012; Kenyon & Bromley 2017a, 2016, 2017c) lead to replenishment of grains in the disk – where large objects break into smaller ones, and gradually are removed by radiation pressure and accretion. The debris disks might give rise to dynamical excitations and perturbations of mass that will eventually drive matter onto the WD within the disk lifetime (Girven et al. 2012; Veras & Heng 2020). Poynting-Robertson drag results from the radiation force and causes loss of angular-momentum for small pebbles, carrying them to the WD (Burns et al. 1979; Rafikov 2011a,b).

The dynamics and architecture of WD disks are similar to protoplanetary disks in some aspects, and different in others. While there are some processes that take place in both of them, such as fragmentation, their parameters might differ significantly. The scales of WD disks are much smaller, the density and temperature profiles are different, and the typical velocities could be much higher.

One important process in protoplanetary disks is wind erosion. wind erosion is a purely mechanical destructive process, which is very common in many occasions in nature, mainly discussed in the context of sand dunes (Bagnold 1941). Recently, we showed that wind erosion can play an important role in planet formation by setting a new growth-barrier for pebbles/boulders in protoplanetary disks, and affecting pebble accretion and streaming instability (Grishin et al. 2020; Rozner et al. 2020). wind erosion in protoplanetary disks is rapid and efficient, as also verified in lab experiments and numerical

* E-mail: morozner@campus.technion.ac.il
† STFC Ernest Rutherford Fellow

© 2020 The Authors
simulations of the conditions of protoplanetary disks (Paraskov et al. 2006; Demirci et al. 2020b; Demirci & Wurm 2020; Demirci et al. 2020a; Schaffer et al. 2020). Wind erosion leaves signatures on the dynamics of objects in the disk, e.g. it fuels pebble-accretion and induces a redistribution of sizes in the disk, and might potentially lead to reshaping or complete destruction of objects (Grishin et al. 2020) along with wind erosion, and accelerate the destruction of small objects.

In this paper, we suggest that wind erosion could take place on WD disks and interact symbiotically with other dynamical processes in the disk. In fact, we show that for certain regimes, for objects smaller than the sublimation radius, $\Sigma_{g,0}$ is the fiducial surface density and $\beta$ is an arbitrary exponent which is parametrized as $\beta = n + 1/2$, where $n$ describes the viscosity power law $\nu(a) \propto a^n$. The gas density $\rho_g$ is determined by the surface density, $\rho_g = \frac{\Sigma_g}{2h(a)}$, (2)

where $h$ is the height of the disk.

This scaling of $\beta$ also induces a temperature scaling (Metzger et al. 2012),

$$T(a) \propto \begin{cases} \text{constant}, & n = 3/2; \\ a^{-1/2}, & n = 1 \end{cases}$$

(3)

where $n = 3/2$ corresponds to an optically thick disk, and $n = 1$ corresponds to an optically thin disk. The aspect ratio of the disk is loosely constrained and strays over some orders of magnitude. We will use an aspect ratio of $10^{-2}$ unless stated otherwise.

The lifetime of WD disks (at least the ones within a couple of Solar radii from the WD) ranges between $\sim 10^3 - 10^6$ yr (Girven et al. 2012; Veras & Heng 2020). Unless stated otherwise, we will use $n = 3/2$ for all our profiles.

### 3 WIND EROSION & THERMAL DESTRUCTIVE PROCESSES IN DISKS

#### 3.1 wind erosion

Consider a spherical object with radius $R$ that resides at a constant distance $a$ from the WD and is built from grains with a typical size $d$, that move in a gaseous medium with a density $\rho_g$. The pressure support present in gaseous disks leads to a difference between the Keplerian velocity around the WD $\Omega_K$ and the actual angular velocity $\Omega_g$, $\Omega_K - \Omega_g = (2\Omega_K a \rho_g)^{-1} \partial P/\partial r$ where $\partial P/\partial r$ is the pressure gradient. Furthermore, the pressure support leads to the radial drift, which presents one of the fundamental problems in planet formation in protoplanetary disks – the meter-size barrier (Weidenschilling 1977).

The radial velocity in protoplanetary disks obtains a maximum for $\sim 1m$ size objects, and these objects inspiral to the inner parts of the disk on timescales shorter than the expected growth timescale. The drift velocity is lower for smaller objects – they are better coupled to the gas and hence have slower relative velocities; larger objects are loosely coupled to the gas and experience slower drift velocities.

For objects in WD disks, the maximal drift velocity is obtained for smaller objects, in size $\lesssim 1$ cm (Kenyon & Bromley 2017c).

$$v_{rel,\psi} = \frac{-2\eta v_k St}{1 + St^2},$$

(4)

$$v_{rel,\phi} = -\eta v_k \left( \frac{1}{1 + St^2} - 1 \right)$$

(5)

where the Stokes number is defined by

$$St = \Omega_K t_{stop},$$

(6)

$$t_{stop} = \frac{m v_{rel}}{F_D}$$

(7)

where $m$ is the mass of the object, $F_D$ is the drag force, which is given by

$$F_D = \frac{1}{2} C_D (Re) \pi R^2 \rho_g v_{rel}^2$$

(8)

In contrast with protoplanetary disks which properties are better-constrained, WD disk parameters are uncertain by orders-of-magnitude. Here we briefly review the ranges of these parameters that will be used in the rest of the paper.

The total mass of a WD disk ranges between $10^{12} - 10^{25}g$ (see a detailed discussion in Metzger et al. 2012; Veras & Heng 2020 and references therein). The mass of the gas in the disk, parametrized by the gas-to-dust ratio, is highly unconstrained and ranges between $10^{-5}$ and unity (Veras 2016). Observations set the lower limit of the inner-radius to be $\lesssim 0.2R_\odot$ (e.g. Rafikov 2011a) and the outer-radius to be $\gtrsim 1.2R_\odot$ (e.g. Gansicke et al. 2006).

The surface density profile is given as (Metzger et al. 2012),

$$\Sigma_g(a) = \Sigma_{g,0} \left( \frac{a}{R_g} \right)^{-\beta} \left( \frac{M_{\text{disk}}}{10^{24}g} \right),$$

(1)

where $a$ is the distance from the center of the disk, $R_g = 2\times10^{10}$ cm

is the sublimation radius, $\Sigma_{g,0}$ is the fiducial surface density and $\beta$ is an arbitrary exponent which is parametrized as $\beta = n + 1/2$, where $n$ describes the viscosity power law $\nu(a) \propto a^n$. The gas density $\rho_g$ is determined by the surface density,

$$\rho_g = \frac{\Sigma_g}{2h(a)},$$

(2)

where $h$ is the height of the disk.

This scaling of $\beta$ also induces a temperature scaling (Metzger et al. 2012),

$$T(a) \propto \begin{cases} \text{constant}, & n = 3/2; \\ a^{-1/2}, & n = 1 \end{cases}$$

(3)

where $n = 3/2$ corresponds to an optically thick disk, and $n = 1$ corresponds to an optically thin disk. The aspect ratio of the disk is loosely constrained and strays over some orders of magnitude. We will use an aspect ratio of $10^{-2}$ unless stated otherwise.

The lifetime of WD disks (at least the ones within a couple of Solar radii from the WD) ranges between $\sim 10^3 - 10^6$ yr (Girven et al. 2012; Veras & Heng 2020). Unless stated otherwise, we will use $n = 3/2$ for all our profiles.

### 2 WHITE DWARF DISKS

In contrast with protoplanetary disks which properties are better-constrained, WD disk parameters are uncertain by orders-of-magnitude. Here we briefly review the ranges of these parameters that will be used in the rest of the paper.

The total mass of a WD disk ranges between $10^{12} - 10^{25}g$ (see a detailed discussion in Metzger et al. 2012; Veras & Heng 2020 and references therein). The mass of the gas in the disk, parametrized by the gas-to-dust ratio, is highly unconstrained and ranges between $10^{-5}$ and unity (Veras 2016). Observations set the lower limit of the inner-radius to be $\lesssim 0.2R_\odot$ (e.g. Rafikov 2011a) and the outer-radius to be $\gtrsim 1.2R_\odot$ (e.g. Gansicke et al. 2006).

The surface density profile is given as (Metzger et al. 2012),

$$\Sigma_g(a) = \Sigma_{g,0} \left( \frac{a}{R_g} \right)^{-\beta} \left( \frac{M_{\text{disk}}}{10^{24}g} \right),$$

(1)

where $a$ is the distance from the center of the disk, $R_g = 2\times10^{10}$ cm
For the drag coefficient, we adopted the fitting used in Perets & Murray-Clay (2011)

\[ C_D(\text{Re}) = \frac{24}{\text{Re}} (1 + 0.27\text{Re})^{0.43} + 0.47 \left[ 1 - \exp \left( -0.04\text{Re}^{0.38} \right) \right] \]  

where Re is the Reynolds number, defined by

\[ \text{Re} = \frac{4Rv_{\text{rel}}}{\nu_{g,d}}, \]  

where \( v_{\text{rel}} = (8/\pi)^{1/2}c_s \) is the mean thermal velocity, \( c_s = \sqrt{k_B T / \mu} \) is the speed of sound, \( k_B \) is Boltzmann constant, \( T \) is the temperature of the disk, \( \mu \) is the mean molecular weight, taken to be \( 2.3m_H \) (following Perets & Murray-Clay 2011) with \( m_H \) the mass of a hydrogen atom and \( \lambda = \mu/(\rho_m \sigma) \) is the mean free path of the gas.

Objects in gaseous disks experience gas drag, which depends strongly on their velocity relative to the gas, \( v_{\text{rel}} \). The gas-drag can play the role that is usually played by the wind in wind erosion and trigger loss of the outer layer of objects, as long as they reach the threshold conditions.

The threshold velocity is dictated by the balance between cohesion forces, self-gravity and gas-drag. The threshold velocity is given by

\[ v_* = \sqrt{\frac{A_N}{\rho_g} \left( \rho_p d^2 + \frac{\gamma}{d} \right)}, \]  

where \( A_N = 1.23 \times 10^{-2} \), and \( \gamma = 0.165 \text{ g s}^{-2} \) are determined empirically from Shao & Lu (2000). Both of them are intrinsic characteristic of the materials that rise from the cohesion forces that hold the particles together – mostly electrostatic forces and van der Waals forces. The gravitational acceleration is \( g = Gm/R^2 \). Above the threshold velocity, i.e. \( v_{\text{rel}} > v_* \), the wind erosion rate is given by (Rozner et al. 2020),

\[ \frac{dR}{dt} = -\frac{\rho_p v_{\text{rel}}^3}{4\pi \rho_p \sigma_{\text{coh}}} \]  

where \( \sigma_{\text{coh}} \) is the cohesion acceleration. The derivation rise from the work done on the eroded object by the shear pressure; see a detailed derivation in Rozner et al. (2020).

3.2 Thermal Destructive Processes

Along with wind erosion, the high temperatures that are usually found in WD disks might give rise to destructive thermal processes such as thermal ablation (Podolak et al. 1988; Pollack et al. 1996; D’Angelo & Podolak 2015) and sublimation (e.g. Metzger et al. 2012; Shestakova et al. 2019). The heat that the outer layer absorbs might lead to phase transitions and then mass loss. There are two regimes, separated by a critical temperature \( T_{\text{cr}} \), in which the latent heat required for vaporization is zero, and varies according to the material (e.g. Opik 1958; Podolak et al. 1988; D’Angelo & Podolak 2015). See the fiducial parameters for ablation in table A.

Below the critical temperature, the rate in which vaporization removes mass is dictated by Hertz-Knudsen-Langmuir equation; see a discussion in D’Angelo & Podolak (2015). In this regime, wind erosion significantly dominates for our choice of parameters, and the timescale for thermal ablation below the critical temperature is \( \approx 95 \text{ yrs} \) – much longer than typical wind erosion timescale, which enables us to neglect the thermal effect and focus on the mechanical processes.

Above the critical temperature, the contribution from thermal processes might add a significant contribution to wind erosion and should be added to eq. 12; assuming blackbody emission, the thermal ablation term is given by

\[ \frac{dR}{dt} = \frac{1}{L_s \rho_p} \sigma_{SB} (T_{\text{cr}}^4 - T_g^4), \]  

where \( \sigma_{SB} \) is the thermal emissivity of the object (\( \sigma_{SB} = 1 \) for a perfect blackbody), \( L_s \) is the particle specific vaporization energy, \( T_{\text{cr}} \) is the critical temperature – which depends on composition of the material – and \( T_g \) is the gas temperature. At high enough temperatures, close to the WD, small grains sublimate to gas (e.g. Metzger et al. 2012; Shestakova et al. 2019).

4 RESULTS

In this section we present the evolution of objects in WD disks due to wind erosion and thermal ablation, starting from a fiducial set of parameters and then vary them.

Wind erosion in WD disks is quite efficient, as manifested in Fig. 1. The timescales for wind erosion are extremely short, and for a constant distance \( a = 0.005\text{AU} = 1R_\odot \) from the WD, objects with radii as large as \( \approx 5 \times 10^5 \text{cm} \) are eroded within the expected disk lifetime. The chosen fixed distance from the WD, along with the rest of the parameters that we don’t vary currently, dictates the final size to which objects are ground down – from \( \approx 0.01\text{cm} \) for 0.001\text{AU} to \( \approx 0.18\text{cm} \) for 0.005\text{AU}.

The final size is determined by the initial conditions of the eroded object, and induces a size re-distribution according to distance from the WD. The outer parts of the disk are more dilute then the inner ones, and since the rate of wind erosion is proportional to the gas density, as can be seen in Eq. 12, wind erosion is more efficient in the inner part of the disks, which leads to shorter timescales and smaller final sizes. Wind erosion has a Goldilocks region of sizes in which it attains its maximal efficiency, since the relative velocity, which plays a significant role in this process, varies with the coupling of objects to the gas.

4.1 Eccentric Orbits

Wind erosion depends strongly on the relative velocity (to the third power), as can be seen from Eq. 12. Henceforth, its effects on objects on eccentric orbits may differ substantially from the effects in the circular case, and lead to stronger more significant erosion due to the higher velocities involved, that might even be supersonic and under some conditions lead to the prompt disruption of objects (Demirci et al. 2020a).

The velocity of a planetesimal in an eccentric orbit is given by

\[ v_p = v_k \sqrt{\frac{2 - r/a}{a}} \]  

where \( M \) is the mass of the WD, \( v_k \) is the Keplerian velocity, \( r \) is the distance and \( a \) is the semimajor axis.

Assuming a circular disk, the gas moves with a velocity

\[ v_g = v_k \sqrt{1 - \frac{n}{a}} \]
The time evolution of objects embedded in a WD disk due to wind erosion. Left: Evolution at a constant distance $a_0 = 0.005$ AU from the WD. Right: Different distances from the WD, with a constant initial size of embedded objects $R_0 = 10^3$ cm.

The effect of wind erosion on an $10^3$ cm object embedded in a WD disk at a distance of $1 R_\odot$ from the center of the WD. The relative velocity of the object is considered as the maximal velocity in the orbit.

The magnitude of the relative velocity between the gas and the planetesimal is given by

$$v_{\text{rel}} = |\hat{v}_p - \hat{v}_g| = \sqrt{v_p^2 + v_g^2 - 2 v_p v_g \hat{v}_g \cdot \hat{v}_p}.$$  \hspace{1cm} (16)

For simplicity, we will assume that the evolution of objects experiencing wind erosion is dominated by the maximal relative velocity in the orbit, when the phase between the gas and the objects is maximal – $\pi/2$, and also assume that the object is at the pericenter, i.e. $r = r_p = a(1 - e)$. See Mai et al. (2020) for more detailed results.

Motion in eccentric orbits shortens the timescales of wind erosion and the final size of eroded objects is smaller and could attain $\sim 0.08$ cm for $e = 0.9$.

4.2 Multilayer Objects

Previously, we discussed objects which are composed from a single-size grain distribution. However, the physical reality might be more complicated and could give rise to a non-trivial internal size distribution. In the following we relax homogeneous composition assumption, and consider the effects of wind erosion on inhomogeneous objects. To the best of our knowledge no previous study considered the internal structure of grains within WD disks, and we adopt internal size distribution models usually considered for asteroids.

The Brazil nut effect in asteroids (Matsumura et al. 2014) suggests that in a mixture of particles, the larger ones tend to end up on the surface of objects. Therefore, when this process acts, the inner structure of an asteroid is such that the larger grains are in the outer layers.

In Figs. 3, 4, we present how differentiated objects react to wind erosion. Erosion enables us to decompose the layers of an object – as far as they are in the correct regimes in which erosion is effective – and to reveal the inner layers in short timescales. Since different sizes of grains impose different rates of wind erosion, the total wind erosion timescales change such that considering larger grains shortens the timescales, and smaller grains lengthen them. Moreover, it can be seen that the final size is determined by the innermost layer, and larger grains lead to smaller final sizes.

4.3 Thermal Effects

At high temperatures, thermal processes become more significant and might strengthen the effect of wind erosion and give rise to further destruction and shorten the timescales.

As can be seen in Fig. 5, thermal ablation shortens the timescales in which objects are ground down to their final scales – here manifested for icy objects. Rocky objects will require higher disk temperatures for thermal ablation to be significant, since the critical temperature for rock is $4000K$; due to the large range of possibilities for WD disks in general – and for temperatures in particular – the temperature in the disk might even exceed the critical temperature for rocks and...
5 DISCUSSION & IMPLICATIONS

5.1 Parameters dependence

The possible parameter range for WD disks is wide and enables us to study a multitude of combinations of parameters. Here we will present a parameter space exploration for solid bodies embedded in WD disks and subjected to the effects of wind erosion.

In Fig. 6 we examine the dependence of wind erosion on the disk mass. As can be seen in eq. 1, the surface density of the disk, and henceforth the gas density, grow linearly with the disk mass. Since the the wind erosion rate is proportional to the gas density, the rate becomes stronger for larger disk masses.

In Fig. 7, we present the dependence of wind erosion on the aspect ratio. Higher aspect ratios lead to stronger wind erosion. And in our default choice of parameters, the aspect ratio should be \( \lesssim 10^{-3} \) in order to maintain significant wind erosion.

5.2 Symbiotic Relations with Other Processes in The Disk

5.2.1 Collisional Cascade

Fragmentational collisional erosion is another destructive process that gradually diminishes the mass of objects in WD disks. This destructive process generates a collisional cascade which grinds down objects to smaller sizes within a certain timescale. Collisional cascades and wind erosion both cause objects to lose mass, such that in the presence of gas, these two processes are symbiotic.

The wind erosion timescale is given by

\[
\tau_{\text{erosion}} = \frac{4\pi R^2 \rho_p a_{\text{coh}}}{\rho_g v_{\text{rel}}}.
\]  

The fragmentation timescale is estimated from the collisional timescale. The collision timescale for a mono-disperse swarm is given by (Kenyon & Bromley 2017b,c and references therein)

\[
t_0 = \frac{r_0 \rho P}{12\pi \Sigma_g},
\]

where \( r_0 \) is the radius of all the objects in the swarm, \( \rho_p \) is their density, \( P \) is their orbital period and \( \Sigma_g \) is the initial surface density. When a multi-disperse swarm is considered, the modification of the timescale is parametrized by a collision parameter \( \alpha_c \equiv v^2 / Q_D \), where \( v \) is the collision velocity and \( Q_D \) is the binding energy of the object (see Leinhardt & Stewart 2012 and references therein), such that the timescale from multi-species is given by \( \tau_c = \alpha \tau_0 \), which can be longer by orders of magnitudes compared with the mono-disperse collision timescales. When the replenishment is efficient enough,
the background distribution of objects remains roughly constant. However, generally, the background density changes with time as well, adding complications to the analysis.

The ratio between the timescales of wind erosion and fragmentational collisions is given by

\[ \frac{t_{\text{erosion}}}{t_{\text{fragment}}} = \frac{96a_e^2 h_{\text{coh}}}{\alpha_e P_{\text{rel}}^3} \frac{R}{\alpha_e P_{\text{rel}}} R \]  

such that the timescales are comparable for a ratio around unity. From equating the ratio to unity, one can set the transition radius between the wind erosion dominated regime and the collisional fragmentation dominated regime, which depends on the rest of the parameters.

In Fig. 8, we compare the typical timescales of wind erosion and fragmentational collisions at which objects are destroyed. For the fragmentation collision timescales, we consider a swarm with a maximal size given by \( R_{\text{max}} \), and assume for simplicity that the fragmentation of intermediate objects (i.e., not the largest or the smallest object in the swarm) starts just when they become the largest of the swarm, which is justified by the hierarchical character of the fragmentational cascade. For the background distribution, we assume a power law distribution of \( N(r) \sim r^{-3.5} \) (Kenyon & Bromley 2017a), and a value of \( v^2 Q_D^2 \) that yields \( \alpha_e \sim 10^2 \), wind erosion dominates at small sizes, and fragmentational collisions at larger sizes. The transition point between the regimes varies with the distance from the WD, such that the regime of wind erosion grows with smaller distances. The wind erosion timescales are very short in these regimes, but might be comparable to or longer than the orbital period timescales of the objects.

We would like to stress that although the destructive character of both wind erosion and collisional cascades leads to shrinkage of objects in the disks, they differ by their intrinsic physical mechanisms. Wind erosion originates from shear pressure that is induced by gas drag. Hence, the presence of gas in the disk is a necessary condition to initiate this process. The collisional cascade arises from collisions between particles in the disk.

5.2.2 External Seeding of Objects into The Disk

The abundance of large objects in WD disks might be replenished as a result of seeding (Grishin et al. 2019; Grishin & Veras 2019). Exo-planetesimals from external sources could enrich the abundance of objects in the disk that will eventually be eroded. External capture especially contributes to the number of large objects, although the total captured mass is small compared to the dust initial abundance. Furthermore, seeding could bring into the disk new materials that might eventually end as pollutants on the WD. The capture rate is dictated by the supply rate and the capture probability; both vary with the origin and the size of the captured objects.

The captured objects change the size distribution in the disk, and might contribute to the steady-state distribution. The injection of external objects might be at a sufficient rate to cancel out the destructive processes and maintain a distribution with larger objects than expected. The revised size distribution should be derived from a full swarm simulation which includes collisional cascade, wind erosion, growth and seeding.

5.2.3 Further Disk Generations

The parameters and characteristics of the disk might vary from one generation to another. Wide-binary evolution could lead to an evolved donor that transfers mass to its companion, such that the captured material forms a disk (Perets 2010; Perets & Kenyon 2013; Schleicher & Dreizler 2014; van Lieshout et al. 2018). A binary main-sequence system evolves such that the more massive star sheds material which is accreted on the secondary and forms a protoplanetary disk; the mass that is lost from the system, which is much greater than the mass transferred from one star to the other, leads to expansion of the binary orbit (Veras et al. 2011; Kratter & Perets 2012; Veras & Tout 2012). Afterwards, a second generation of debris and planets form in the pre-evolved system, such that the secondary evolves off the main-sequence and sheds material to its WD companion and a protoplanetary disk formed – similarly to the previous stages. Finally, the binary orbit expands and a third generation debris disk is formed.

Higher generation disks might give rise to different disk composition, since metallicity varies from one generation to another, such that the formed accretion disks are metal and dust rich. Higher metallicity environments are better for planet formation (Fischer & Valenti 2005), such that the formed disks are likely to have planetary and planetesimal structures.

5.3 Possibilities for wind erosion of SDSS 1288+1040 b

One notable potential application of wind erosion theory is the disk orbiting the WD SDSS J1228+1040 (Manser et al. 2019). This disk contains a planetesimal on an orbit with \( a = 0.73R_\odot \) and \( e \approx 0.54 \). This orbit is fully embedded in a dusty and gaseous planetary debris disc, which extends beyond \( 1R_\odot \).

Because of this compact planetesimal orbit, and because the planetesimal has been observed over at least 4,000 orbits, it cannot represent a typical rubble-pile solar system asteroid. Instead, it likely represents an iron-rich remnant core of a planet, and harbours nonzero internal tensile strength. The internal structure and size are poorly constrained: the estimated radius range is \( R = 1.2 \sim 120 \text{ km} \).

Hence, for only the lowest end of this size range could wind erosion be effective. Figure 1 illustrates that km-sized objects may be eroded in timescales under \(~ 10^6 \text{ yr} \). However, the structures of the objects in that figure are likely to be very different than the strong and dense planetesimal around SDSS 1228+1040. Furthermore, a potentially competing effect are bodily gravitational tides. Veras et al. (2019) show that these tides could instigate a WD to engulf objects containing just \( 10^{-3} M_\odot \), but only for objects with sufficiently low internal viscosities.
wind erosion is a very effective process in WD disks, as long as the amount of gas in the disk is non-negligible. The current observations of WD disks with a gaseous component cannot yet well constrain several of the disk parameters, such as the disc mass and its scale height. Also, the exact origins of the gas in such disk are not well understood, with suggested origins include sublimation (e.g. Metzger et al. 2012), grain-grain collisional vaporization and sputtering.

Along with the destructive processes, there could be mass influx that we did not take into consideration in this paper. As manifested in Kenyon & Bromley (2016, 2017c) in the context of collisional cascade, the rate of mass input might equalize the mass loss such that objects that are a-priori expected to be pulverized and will maintain their mass for long timescales. However, here the combined effect of fragmentational erosion and wind erosion might play a role, and these two processes together will lead to mass depletion of objects.

We have neglected any asphericity in the object, which is assured due to the lack of perfect packing efficiency of its constituent grains. Furthermore, we have neglected any asphericity that develops as a result of an wind erosion, which acts in the direction of the headwind, and might reshape the eroded objects.

7 SUMMARY

The growing number of WD disks (both gaseous and non-gaseous) that have been observationally detected and characterized leave open the possibility for constraining theoretical models for the origins and evolution of such disks. However, even at the theoretical level, there are important gaps in our physical understanding of the dynamics and processes that take place in WD disks.

In this paper we focused on the processes of wind erosion, which, to date, were not considered in the context of WD disks. We made use of an analytical model for wind erosion in WD disks, based on our studies of such processes in protoplanetary disks as presented in Rozner et al. (2020). We find that the typical timescales of wind erosion in WD disks are extremely short, with wind erosion grinding down even km-size objects within the disk lifetime. Consequently, such processes are likely to play an important role in the evolution of small solid bodies in the disk. We also studied the relationship between wind erosion and other physical processes in WD disks and its amplification due to the combined effect (see subsections 3.2, 5.2). Along with collisional cascade and thermal ablation, wind erosion grinds down efficiently large objects into small ones with a characteristic final size. The eroded objects experience dynamical processes that finally grind down planetesimals/rocks/pebbles/boulders into sufficiently small particles such that these could drift towards the WD via Poynting-Robertson drag and contribute to its pollution.

wind erosion is the most efficient and becomes the dominant destruction process for small objects, and the critical radius for its dominance is determined by the parameters of the disk, the physical characteristics of the eroded objects, the distance from the WD and the parameters of the collisional cascade (see eq. 19).

Similarly to protoplanetary disks, wind erosion in WD disks induces a re-distribution of particles size, according to the distance of the particles from the WD. Henceforth, wind erosion sets constraints on the parameters of WD disks that might narrow down the current parameter space. Due to the extremely short timescales of wind erosion, it is not likely that observable variations in WD disks would be explained by replenishment from wind erosion.

ACKNOWLEDGMENTS

MR and HBP acknowledge support from the Minerva center for life under extreme planetary conditions, the Lower Saxony-Israel Niedersachsisches Vorab research cooperation fund, and the European Union’s Horizon 2020 research and innovation program under grant agree- ment No 865932-ERC-SNeX. DV gratefully acknowledges the support of the STFC via an Ernest Rutherford Fellowship (grant ST/P003850/1).

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

REFERENCES

Bagnold R. A., 1941, The physics of blown sand and desert dunes., Methuen, London
Bonsor A., Carter P. J., Hollands M., Gänssicke B. T., Leinhardt Z., Harrison J. H. D., 2020, MNRAS, 492, 2683
Burns J. A., Lamy P. L., Soter S., 1979, Icarus, 40, 1
D’Angelo G., Podolak M., 2015, ApJ, 806, 203
Demirci T., Wurm G., 2020, arXiv e-prints, p. arXiv:2007.12074
Demirci T., Schneider N., Teiser J., Wurm G., 2020a, arXiv e-prints, p. arXiv:2010.14368
Demirci T., Schneider N., Steinpilz T., Bogdan T., Teiser J., Wurm G., 2020b, MNRAS, 493, 5456
Dennihy E., et al., 2020, arXiv e-prints, p. arXiv:2010.03693
Doyle A. E., Young E. D., Klein B., Zuckerman B., Schlichting H. E., 2019, Science, 366, 356
Farihi J., 2016, New Astron. Rev., 71, 9
Farihi J., et al., 2018, MNRAS, 481, 2601
Fischer D. A., Valenti J., 2005, ApJ, 622, 1102
Gänssicke B. T., Marsh T. R., Southworth J., Rebassa-Mansergas A., 2006, Science, 314, 1908
Gentile Fusillo N. P., et al., 2020, arXiv e-prints, p. arXiv:2010.13807
Girven J., Brinkworth C. S., Farihi J., Gänssicke B. T., Hoard D. W., Marsh T. R., Koester D., 2012, ApJ, 749, 154
Grishin E., Veras D., 2019, MNRAS, 489, 168
Grishin E., Perets H. B., Avni Y., 2019, MNRAS, 487, 3324
Grishin E., Rozner M., Perets H. B., 2020, ApJ, 898, L13
Harrison J. H. D., Bonsor A., Madhusudhan N., 2018, MNRAS, 479, 3814
Hollands M. A., Gänssicke B. T., Koester D., 2018, MNRAS, 477, 93
Jura M., 2008, AJ, 135, 1785
Jura M., Young E. D., 2014, Annual Review of Earth and Planetary Sciences, 42, 45
Kenyon S. J., Bromley B. C., 2016, ApJ, 817, 51
Kenyon S. J., Bromley B. C., 2017a, ApJ, 839, 38
Kenyon S. J., Bromley B. C., 2017b, ApJ, 844, 116
Kenyon S. J., Bromley B. C., 2017c, ApJ, 850, 50
Koester D., Gänssicke B. T., Farihi J., 2014, A&A, 566, A34
Krautter K. M., Perets H. B., 2012, ApJ, 753, 91
Krus M., Musiolik G., Demirci T., Wurm G., Teiser J., 2019, arXiv e-prints, p. arXiv:1911.01692
Leinhardt Z. M., Stewart S. T., 2012, ApJ, 745, 79
Mai C., Desch S. J., Kuiper R., Marleau G.-D., Dullemond C., 2020, ApJ, 899, 54
Malamud U., Perets H. B., 2020a, MNRAS, 492, 5561
Malamud U., Perets H. B., 2020b, ApJ, 849, 698
Manser C. J., et al., 2019, Science, 364, 66
Manser C. J., Gänssicke B. T., Gentile Fusillo N. P., Ashley R., Breedt E., Hollands M., Izquierdo P., Pelisoli I., 2020, MNRAS, 493, 2127
Matsumura S., Richardson D. C., Michel P., Schwartz S. R., Ballouz R.-L., 2014, MNRAS, 443, 3368

MNRAS 000, 1–8 (2020)
APPENDIX A: TABLE OF COMMONLY USED PARAMETERS

In this appendix, we present the default values for the used parameters, unless stated otherwise.

This paper has been typeset from a \TeX/\LaTeX file prepared by the author.
| Symbol | Definition | Fiducial Value | Reference |
|--------|------------|----------------|-----------|
| $\gamma$ | 0.165g/sec$^2$ | [Kruss et al. (2019)](https://example.com) |
| $A_N$ | $1.23 \times 10^{-2}$ | [Shao & Lu (2000)](https://example.com) |
| $\beta$ | $10^2$ g s$^{-1}$ | scaled from [Paraskov et al. (2006)](https://example.com) and references therein |
| $\rho_p$ | planetsimals' density | rock $3.45$g cm$^3$, ice $1.4$g cm$^3$ | [Pollack et al. (1996)](https://example.com) |
| $\mu$ | mean molecular weight | $3.85 \times 10^{-24}$ g | [Perets & Murray-Clay (2011)](https://example.com) |
| $\sigma$ | neutral collision cross-section | $10^{-15}$ cm | [Perets & Murray-Clay (2011)](https://example.com) |
| $T$ | temperature (optically thick) | 1000K | |
| $\rho_\text{planetesimals}$ | planetesimals' density | scaled from [Paraskov et al. (2006)](https://example.com) and references therein |
| $\mu$ | mean molecular weight | $3.85 \times 10^{-24}$ g | [Perets & Murray-Clay (2011)](https://example.com) |
| $\sigma$ | neutral collision cross-section | $10^{-15}$ cm | [Perets & Murray-Clay (2011)](https://example.com) |
| $T$ | temperature (optically thick) | 1000K | |
| $M_{\text{disk}}$ | disk mass | $10^{24}$ g | [Grishin & Veras (2019)](https://example.com) |
| $\Sigma_g$ | surface density profile (optically thick) | $51 \times 10^3$ g cm$^2$ | |
| $h/r$ | aspect ratio | $10^{-2}$ | [Podolak et al. (1988)](https://example.com) |
| $d$ | typical 'building-block' grain size | 0.1 cm | [Podolak et al. (1988)](https://example.com) |
| $R_s$ | sublimation radius | $10^{10}$ cm | [Rafikov (2011a)](https://example.com) |
| $T_\text{cr}$ | critical temperature | ice 648K, rock 4000K | |
| $L_\sigma$ | particle specific vaporization energy (solid) | ice $2.83 \times 10^{10}$ erg g$^{-1}$, rock $8.08 \times 10^{10}$ erg g$^{-1}$ | [D'Angelo & Podolak (2015)](https://example.com) |