Experimental Comparison of Visual and Single-Receiver GPS Odometry

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Abstract—Mobile robots rely on odometry to navigate through areas where localization fails. Visual odometry (VO) is a common solution for obtaining robust and consistent relative motion estimates of the vehicle frame. Contrarily, Global Positioning System (GPS) measurements are typically used for absolute positioning and localization. However, when the constraint on absolute accuracy is relaxed, time-differenced carrier phase (TDCP) measurements can be used to find accurate relative position estimates with one single-frequency GPS receiver. This suggests practitioners may want to consider GPS odometry as an alternative or in combination with VO. We describe a robust method for single-receiver GPS odometry on an unmanned ground vehicle (UGV). We then present an experimental comparison of the two strategies on the same test trajectories. After 1.8km of testing, the results show our GPS odometry method has a 75% lower drift rate than a proven stereo VO method while maintaining a smooth error signal despite varying satellite availability.

I. INTRODUCTION

Odometry is an important component of almost any mobile robotic navigation strategy; it takes many forms including visual, visual-inertial, lidar, and wheel odometry. All of these use different sensors to accomplish the common goal of estimating the vehicle’s path or trajectory. In mapping, odometry allows local reconstruction of the environment and in localization it is critical to the success of autonomous navigation systems such as Visual Teach and Repeat (VT&R) [1]. In experience-based navigation (EBN) [2] and multi-experience localization (MEL) [3], odometry is used to bound pose uncertainty in short sections (i.e., less than 50m) where localization fails due to factors such as appearance change. If odometry drift becomes too large, the robot may not be able to navigate safely. This is in turn causes a missed opportunity to improve the map. Better odometry allows a robot to dead-reckon for longer sections and therefore drive further successfully.

One idea to improve a robot’s odometry is to consider other sensors. Single-frequency Global Positioning System (GPS) receivers are now ubiquitous, coming standard in almost every smartphone. First operational in 1983 [4], GPS allows an absolute positioning solution to be calculated anywhere on Earth with a clear view of the sky. Since then, other Global Navigation Satellite Systems (GNSS) constellations such as GLONASS, Galileo, and BeiDou have come online and may be used independently or in combination with GPS. GNSS has become an important tool for mobile robotic navigation. However, standard pseudorange GNSS positioning does not have the accuracy required to bound vehicle travel within the envelope required for visual localization, which typically degenerates with decimetre-level lateral errors [1].

Utilizing other GNSS observables over short windows of time can improve relative positioning. Figure 1 illustrates the relative accuracy of three different single-receiver odometry strategies over a short trajectory. In this paper, we demonstrate the use of time-differenced carrier phase (TDCP) measurements as an odometry solution for an unmanned ground vehicle (UGV).

We compare the performance of single-receiver GPS odometry with stereo visual odometry (VO) on the same set of test trajectories. To the best of our knowledge this is the first study comparing and contrasting TDCP with VO. Our results, previewed in Figure 1 and discussed in Section V, show TDCP is a worthy alternative to VO in outdoor applications. We also briefly examine the advantages of using both sensors in the same estimator in Section V-C.

II. RELATED WORK

A. Global Navigation Satellite Systems

Standard GNSS positioning involves the trilateration of pseudorange measurements of four or more dedicated positioning satellites. In good conditions, pseudorange-based positioning can achieve accuracy on the order of 1–2m despite several sources of error affecting the signal’s measured time-of-flight [5]. GNSS receivers can also calculate the carrier phase of the signal based on its Doppler shift. These measurements are much less noisy but cannot be used directly due to the unknown integer ambiguity of wavelengths between the receiver and each satellite. Real-time kinetic
We use an implementation of VO developed as a component of VT&R based on parallel tracking and mapping (PTAM) [20]. Motion estimates are computed at framerate while landmark positions are optimized after each keyframe. It is fast and reliable with the parameters pre-tuned on data separate from that presented in this work. While testing on nearly 10km of driving over 30 hours, MacTavish et al. [21] found a 1.5% translational drift rate during daytime conditions and a 2.4% rate at nighttime via the use of headlights for this algorithm.

III. METHODOLOGY

A. Coordinate Frames

There are five frames of interest to our optimization problem. The global east-north-up (ENU) frame, \(F_{\text{e}}\), is a stationary frame tangential to the Earth at the vehicle start position. All other frames are transient. The vehicle frame, \(F_{v}\), is located at the centre of the vehicle at axle height. All estimation is computed in \(F_{v}\) before being transformed to the GPS receiver frame, \(F_{r}\), for comparison with ground truth positions. The origin of the satellite frame, \(F_{s}\), is defined at the antenna phase centre (APC) for calculating ranges. Finally, the camera frame, \(F_{c}\), is located at the left camera of the stereo module. The VO algorithm is also configured to output estimates in the vehicle frame.

B. Time-Differenced Carrier Phase

Whereas RTK positioning makes use of carrier phase measurements from two receivers separated in space, TDCP positioning makes use of measurements from a single receiver separated by both time and space. The carrier phase range equation to a single satellite at time \(a\) is given by

\[
\Phi_a = \rho_a + N + c\delta_a^R - c\delta_a^S + E_a + T_a - I_a + m_a + \epsilon_a,
\]

(1)

where \(\Phi_a\) is the measured phase in radians multiplied by the known wavelength so that all values have units of metres. GNSS receivers can measure the incoming phase quite accurately meaning the white noise affecting the measurement, \(\epsilon\), is typically less than 2mm [5]. However, the signal is affected by several sources of systematic error as it propagates from satellite to receiver causing the measured range, \(\Phi\), to differ
from the true range to the satellite, \( \rho \). These include receiver and satellite clock errors (\( \delta R \) and \( \delta T \)), satellite ephemeris error (\( E \)), tropospheric delay (\( T \)), ionospheric affects (\( I \)), and multipath \( m \).

\( N \) is the unknown wavelength ambiguity; if the receiver stays in phase lock with the satellite it is time invariant. We can therefore eliminate it by differencing \( \Phi \) taken at two times, \( a \) and \( b \):

\[
\Phi_b - \Phi_a = \rho_{ba} + c_0 \delta_{ba} - c_0 \delta_{a} + E_{ba} + T_{ba} - I_{ba} + m_{ba} + \epsilon_{ba}. \tag{2}
\]

The subscript \( ba \) denotes the difference between a quantity at time \( b \) and time \( a \). The receiver clock error is typically large so must be dealt with explicitly, either by estimating it or differencing the equation again for two different satellites.

The latter gives our measurement model:

\[
\Phi_{21}^{ba} = \rho_{21}^{ba} - c_0 \delta_{ba}^{21} + E_{21}^{ba} + T_{21}^{ba} - I_{21}^{ba} + m_{21}^{ba} + \epsilon_{21}^{ba}, \tag{3}
\]

where \( \rho_{21}^{ba} \), for example, denotes the double difference \( (\rho_b^2 - \rho_a^2) - (\rho_b^1 - \rho_a^1) \). The ranges making up \( \rho_{21}^{ba} \) are calculated using:

\[
\rho_a = \| \mathbf{r}^{\gamma}_g(t_a) \| = \| \mathbf{r}^{\gamma}_g(t_a) - \mathbf{r}^{\gamma}_g(t_a) \|, \tag{4}
\]

where \( \mathbf{r}^{\gamma}_g \) is the known satellite ephemeris and \( \mathbf{r}^{\gamma}_g \) is our state. It is important to recalculate the ephemeris at each measurement time because the satellites travel at 3.9km/s. From (3), we can write our error term for one pair of satellites seen at one pair of positions as:

\[
e_{21}^{ba} = \Phi_{21}^{ba} - \rho_{21}^{ba}. \tag{5}
\]

Our weighted least squares factor given \( n \) commonly seen satellites at \( t_a \) and \( t_b \) is

\[
J_{ba} = \sum_{k=2}^{n} w_k (e_{k1}^{ba})^2 \tag{6}
\]

where \( w_k \) is a scalar variance parameter, which we set as a constant in our implementation though it could be tuned if more information on the measurement quality from each satellite was known. \( J_{ba} \) is symbolized as a blue dot in Figure 3.

For optimization, a linearized error term is needed and we derive this by noting that \( \mathbf{r}^{\sigma}_g(t_b) \) and \( \mathbf{r}^{\sigma}_g(t_a) \) are approximately parallel for small \( \epsilon_{ba} \). The range to the satellite can change due to both the receiver’s movement and the satellite movement between measurement times. As illustrated in Figure 4 the range difference due to the receiver movement is equal to the negative of the displacement vector projected onto the unit vector to the satellite, \( \mathbf{u} \):

\[
\rho_{ba} = -\mathbf{u}^T (\mathbf{r}^{\sigma}_g(t_b) - \mathbf{r}^{\sigma}_g(t_a)) + \mathbf{u}^T (\mathbf{r}^{\sigma}_g(t_b) - \mathbf{r}^{\gamma}_g(t_a)), \tag{7}
\]

where the second half of the right-hand side is independent of the state. After substituting (7) into our error equation, (5), we can calculate the Jacobian required to perform Gauss-Newton optimization.

### C. Implementation Details

The first step in our trajectory estimation pipeline is to parse the raw phase (logged as binary RTCM1004 messages) and calculate coarse pseudorange positions for initializing our state. Preprocessing was done using the C library RTKLIB [22]. TDCP cost terms were only added between consecutive vertices in the factor graph (defined once per second) using commonly seen satellites that maintained phase lock. This is the “Consecutive” factor graph configuration seen in Figure 3. Because the majority of the error is systematic rather than the white noise, \( \epsilon \), we find, as shown in Traugott [11], that including TDCP constraints over longer timespans as in Suzuki [23] or the “Dense” configuration of Figure 3 has no significant effect on performance besides increased computational cost.

Some of the errors in (1), the phase range equation, can be mitigated through modelling. It is typical to use the Klobuchar model [24] to partially correct for ionospheric...
effects, the parameters of which are available in the GPS navigation message. The Niell mapping function [25] with the UNB3 model parameters [26] can be used to estimate the tropospheric delay. Both models are a function of atmospheric conditions and satellite elevation. Because atmospheric conditions change slowly and the errors are differenced in (7), their impact is lessened compared to the effect on a single phase measurement. However, the effect of satellite elevation change over the time difference can be significant for satellites close to the horizon. In our experiments, we model the tropospheric delay but omit the ionospheric correction because the applicable messages were not logged for all runs. We find the difference in performance to be negligible.

Given enough satellites, TDCP will provide a positioning solution but to be practical for vehicle odometry, and as a fair comparison for VO, we require full $SE(3)$ pose estimates in the vehicle frame. Our algorithm is designed and tested for a nonholonomic robot so constraints that penalize lateral velocity of the vehicle frame are used to resolve vehicle orientation. We also use a white-noise-on-acceleration (WNOA) motion prior [27] to encourage smoothness. Unlike other TDCP algorithms, the use of these motion models allows the robot to make use of carrier phase information and still calculate a state estimate when less than four phase-locked satellites are available. The factor graph can be seen in Figure 3(b).

The optimization is run as a filter (forward-pass only) to simulate online odometry calculations. It is solved with the STEAM [27] implementation of the Dogleg Gauss-Newton algorithm [28] and the motion model applied over a 10-second sliding window. Carrier-phase measurements are subject to outliers so a robust cost function, dynamic covariance scaling (DCS) [29], is used on the TDCP factors.

D. Visual Odometry

Stereo VO pose estimates are computed via the same algorithm used in VTr&L. The odometry pipeline follows a similar strategy as [20] in which one module estimates camera pose with respect to the previous keyframe at framerate while another performs a local windowed bundle adjustment on map landmarks after each keyframe. Sparse speeded-up robust features (SURF) [30] are used with random sample consensus (RANSAC) [31] to detect outliers. The same WNOA motion prior is used as in III-C. The stereo error terms also have a DCS robust cost function applied to them. Relative pose estimates are computed by solving the Gauss-Newton optimization problem with the STEAM solver.

IV. EXPERIMENTAL SETUP

All data was collected aboard the Grizzly Robotic Utility Vehicle (RUV) pictured in Figure 1. The vehicle maintained an average velocity of approximately 1m/s across terrain that included pavement and snow-covered grass at the University of Toronto Institute for Aerospace Studies (UTIAS) campus. Stereo images were captured by a front-facing Point Grey Bumblebee XB3 stereo camera, which has a 24cm baseline, a 66° horizontal field of view and captures 512x384 pixel images at a 16Hz framerate. GPS measurements were recorded by a front-mounted NovAtel SMART6-L receiver. Carrier phase measurements were logged at 1Hz while RTK ground truth was logged separately at 4Hz. The RTK positioning is expected to have a RMS error of 1cm + 1ppm under nominal conditions. Doppler velocities were also logged for comparison.

To first test our GPS odometry, the robot was manually driven on four separate runs over two data collection days during which only GPS data was logged. These results are presented in Figure 4. For the comparison experiment, five independent runs were driven on a third day, each spanning several minutes. These runs were then split into 15 independent 50m sections, approximately equally spaced, for evaluation. We chose 50m as an evaluation distance as we do not anticipate driving a robot on dead reckoning farther than this and it was sufficient for measuring odometry drift rate. As VO does not estimate orientation in the global East-North-Up (ENU) frame, the 10m of trajectory preceding the test section was used for alignment of the VO estimates. The continuous-time trajectories computed by STEAM are used to interpolate the VO estimates to the ground truth GPS timestamps (as they are asynchronous to the VO keyframe timestamps). Evaluation is considered based on the amount of drift (absolute translation error) after 25m and 50m.

V. RESULTS

A. GPS Odometry

Satellite availability for the GPS-only experiment varied throughout the runs as buildings and even the vehicle sensor mast itself caused partial occlusions of the sky. Despite this, the receiver kept enough satellites in phase lock throughout the runs for a consistent position estimate at all times. The
The median number of satellites seen was 7 with the minimum 4 and the maximum 9.

Each 250m trajectory presented in Figure 6 encompasses nearly five minutes of driving – significantly further than a robot would need to rely on dead-reckoning between localizations. We find that the total horizontal translational error after 250m is less than 1m for all runs and the mean error at this point is 0.78m. The errors grow smoothly and approximately linearly. The drift in both the $x$ (East) and $y$ (North) directions is reasonably consistent as we might expect considering the systematic errors affecting the phase measurements in Equation (1). We also find the positioning errors from integrating the Doppler measurements are approximately twice as large as in our TDCP algorithm. The results provide further evidence that TDCP should be preferred over integrated Doppler velocity for estimating relative position with a single receiver.

B. Comparison to Visual Odometry

Figure 7 shows an overhead view of the estimates from both algorithms on three of the test trajectories representative of the larger test set. Even at this macroscopic scale we can see the GPS odometry outperforms VO. Figure 1 depicts both the errors for the individual runs and an average horizontal position error for each algorithm. After 50m, the TDCP method has a smaller translational error than VO on all but one of the 15 test trajectories. VO has a mean final translational error of 1.127m or 2.25% while TDCP does 75% better with a mean error of 0.281m or 0.56%. The results are similar after just 25m, with drift rates of 2.26% and 0.57%, respectively. The variance in drift rate between runs is also a lot higher for VO as can be seen in the spread of data in Figure 1. This implies the expected errors may be more predictable for TDCP.

A similar number of satellites were available for the comparison experiment as in Figure 6-A with the minimum 5, the median 7, and the maximum 9. Figure 8 examines the relationship between mean satellites seen over a trajectory and final error. There is a negative correlation between errors and number of satellites as expected though the relationship is weak ($r = -0.10$). Other factors such as the particular geometry of the satellites, the atmospheric conditions, and the shape of the trajectory may have more influence.

Looking more closely at the VO results, we see the number of feature matches varies somewhat between the two major

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Fig. 5. The Grizzly Robotic Utility Vehicle used for data collection.

Fig. 6. Plot of position errors over the first 250m of the four trajectories in the GPS-only experiment. The drift rate is low and the errors change approximately linearly.

Fig. 7. Overhead view of ground truth and estimates for three of the 15 test trajectories. VO drifts noticeably further from ground truth than the TDCP-based odometry.
for ease of comparison. We find under good conditions the addition of vision does not significantly improve accuracy because the estimates from VO are worse quality. If the uncertainties are improperly set, the inclusion can actually degrade performance. But, using both sensors does improve robustness when the quality or availability of one or both sensors cannot be guaranteed. To show this, we simulate both full (zero satellites available) and partial (two satellites available) temporary GPS dropouts and observe the effect on our odometry with and without the inclusion of VO. The short, 15-second dropouts occur near the beginning of the approximately one-minute long trajectories.

As seen in Figure 8, qualitatively, we get similar estimates with and without VO when sufficient satellites are available throughout. During dropouts, the GPS-only estimator is forced to rely heavily on its motion model and accuracy suffers. Local accuracy does recover once satellites are reacquired. In the partial dropout, the receiver displacement is not fully constrained as only two satellites are available, but our algorithm can still make use of the carrier phase information to some degree and performance is much better than with zero satellites. However, in many applications, the added error would still be considered a failure. With the addition of VO, the performance loss from the dropout is barely noticeable. A combined approach provides the added accuracy of TDCP with the reliability of VO.

VI. CONCLUSIONS AND FUTURE WORK

We simultaneously collected a large set of GPS data and stereo imagery from a ground robot driving outdoors. We evaluated our TDCP-based single-receiver, single-frequency GPS odometry algorithm against a proven stereo VO pipeline in the first known experiment of this kind. The results showed the GPS odometry produced far smaller positional errors with respect to the RTK ground truth. We believe TDCP odometry is a good alternative to VO for outdoor navigation. VO is still preferred in areas where occlusions or other sources of GNSS signal interference are a frequent issue. For added robustness, or in applications such as indoor-outdoor navigation, the two sensors may be combined.

C. Combining GPS and Vision

As our GPS odometry algorithm has been set up as a factor graph, it is amendable to adding factors from other sensors. A natural choice would be to combine the visual and GPS odometry estimators as shown in Figure 3(c) and (d). The results in this section are from a loosely coupled estimator for ease of comparison. We find under good conditions the addition of vision does not significantly improve accuracy because the estimates from VO are worse quality. If the uncertainties are improperly set, the inclusion can actually degrade performance. But, using both sensors does improve robustness when the quality or availability of one or both sensors cannot be guaranteed. To show this, we simulate both full (zero satellites available) and partial (two satellites available) temporary GPS dropouts and observe the effect on our odometry with and without the inclusion of VO. The short, 15-second dropouts occur near the beginning of the approximately one-minute long trajectories.

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One likely way to improve the future performance of our positioning algorithm is to incorporate additional GNSS constellations thereby increasing the number of satellites available. Because the error drift in our estimates is approximately constant throughout a run, it may be possible to estimate and correct for this bias using other sensors. Incorporating TDCP estimates into multi-experience localization (MEL) is a final opportunity for future work of particular interest to us. MEL can fail due to high appearance change. A better odometry solution would allow the robot to safely continue autonomous path traversal while simultaneously logging images to update the map and improve future chances of successful visual localization.

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