Experimental observation of Berry phases in optical Möbius-strip microcavities

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The Möbius strip, a fascinating loop structure with one-sided topology, provides a rich playground for manipulating the non-trivial topological behaviour of spinning particles, such as electrons, polaritons and photons, in both real and parameter spaces. For photons resonating in a Möbius-strip cavity, the occurrence of an extra phase—known as the Berry phase—with purely topological origin is expected due to its non-trivial evolution in parameter space. However, despite numerous theoretical investigations, characterizing the optical Berry phase in a Möbius-strip cavity has remained elusive. Here we report the experimental observation of the Berry phase generated in optical Möbius-strip microcavities. In contrast to theoretical predictions in optical, electronic and magnetic Möbius-topology systems where only Berry phase π occurs, we demonstrate that a variable Berry phase smaller than π can be acquired by generating elliptical polarization of resonating light. Möbius-strip microcavities as integrable and Berry-phase-programmable optical systems are of great interest in topological physics and emerging classical or quantum photonic applications.

The Berry phase (also called the ‘geometric phase’), a non-integrable phase factor originating from a non-trivial evolution of a physical system in parameter space1, plays a fundamental role in various fields ranging from condensed matter physics2–3, acoustics4, high-energy physics5, cosmology6, quantum information7 to optics8. In optics, the Berry phase can be acquired by the non-trivial evolution of either the polarization state or the wave vector in its corresponding parameter space, with purely topological origin8–13. Investigation of the manipulation of polarization states was pioneered by S. Pancharatnam, and the generated geometric phase is now also called the Pancharatnam–Berry phase1,10. Generation of a Berry phase based on wave-vector evolution has been explored by recording polarization rotations in the open light paths of helical14–17 or out-of-plane curvilinear waveguides18. Notably, in recent years, the generation of the topologically protected Berry phase has also been studied in specially designed three-dimensional (3D) optical microcavities with light circulating along a closed path, for example in asymmetric whispering-gallery-mode microcavities19, out-of-plane microrings20 and microrings with embedded angular...

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scatterers\textsuperscript{21}, which show great potential for on-chip integrated topological photonics.

The Möbius strip\textsuperscript{22}—a fascinating loop structure well-known for its one-sided topology—also symbolizes the topological twist of the band structure in topological insulators\textsuperscript{23}. The Möbius topology plays important roles in multiple disciplines, ranging from the generation of symmetry-breaking Möbius soliton modes in a magnetic medium\textsuperscript{24} to the extraordinary behaviour of electronic waves in Möbius aromaticity\textsuperscript{25} and twisted semiconductor strips\textsuperscript{26}, as well as anomalous plasmon modes formed in metallic Möbius nanostructures\textsuperscript{26}. To impose the Möbius topology on photons, the optical field is twisted by liquid-crystal \(\phi\)-plates as cavity-free systems\textsuperscript{27}. However, investigating the topological phenomena of light resonating in a real Möbius-structured cavity remains highly desirable. Very recently, a Möbius-strip cavity composed of a twisted dielectric strip was explored as a platform for the investigation of non-Euclidean optics\textsuperscript{28}. However, the optical Berry phase, the key topological phenomenon, has not been experimentally demonstrated, although the existence of a Berry phase in a Möbius cavity was theoretically predicted a long time ago\textsuperscript{29,30}. Theoretical studies have shown the occurrence of Berry phase \(\pi\) in an ideal Möbius-strip cavity, resulting in constructive self-interference of half-integer number modes (that is, accommodating half-integer numbers of wavelengths) in a closed-path trajectory\textsuperscript{31}. The half-integer number of wavelengths, which has a purely topological origin, contradicts the well-known resonant condition in conventional optical or plasmonic cavities.

The topological behaviour of circulating light in Möbius-strip waveguiding systems has not yet been explored experimentally, preventing achieving new insights into observable optical phenomena for topology-based signal processing and communications. In this Article we report the experimental observation of optical Berry phases occurring in Möbius-strip microcavities with tailored cross-sectional geometry. In contrast to previous theoretical predictions, where only phase \(\pi\) occurs, here we observe and reveal programmable Berry phases ranging from \(\pi\) to 0 for resonant light waves with linear to elliptical polarization, in carefully designed Möbius-strip resonators. As the quantum holonomy, the Berry phase generated in a compact optical Möbius system is particularly promising for geometric quantum mechanics and its applications, such as simulation, metrology, sensing and computation.

Results

Principles

The discussion starts with the optical polarization states in an ideal Möbius strip, in which the strip thickness \(T\) is much smaller than the strip width \(W\) (Fig. 1). Considering linearly polarized light resonating in the Möbius-strip waveguide, the optical electric field is guided and forced to remain in the plane of the twisted strip. Such a twisted-strip waveguide functions similarly to some free-space optical components, such as a half-wave plate\textsuperscript{1} or a Dove prism\textsuperscript{32}, which affect the orientation of the polarization states. As a result, the polarization continuously re-orientates along the twisted strip during propagation, which we term the ‘in-plane’ (IP) mode. The IP mode represents an adiabatic cyclic evolution of linearly polarized light in a smoothly curved waveguide. The acquired phase factor of the light wave can be divided into two parts, the dynamic phase and the Berry phase (alternatively called the geometric phase). The dynamic phase reflects the system’s evolution in time, which is determined by the optical path and the system’s curvature. In contrast, the Berry phase memorizes the evolution path in the parameter space, which is independent of the dynamic phase. Using a phenomenological model, the occurrence of Berry phase in a Möbius strip can be directly visualized by the parallel transport of a vector along the twisted strip. For reference, we investigate a comparable 3D ring cavity (‘curved strip’) with the same curvature as that of a Möbius strip but without the Möbius topology (Supplementary Fig. 1 and Supplementary Note 1). In contrast to the one-sided Möbius strip with a single surface, the curved strip is topologically identical
to conventional microring cavities. As shown in Fig. 1, although the vector orientations are kept in parallel with each other at each local position during transport, the vector flips by an angle $\pi$ after a full trip around the Möbius strip, whereas there is no such a flip in the curved strip.

For the adiabatic cyclic evolution of a degenerate physical system there are usually two analytical ways to quantify the occurring Berry phase via the corresponding solid angle in parameter space. One way is determined by the wave vector $k$, which forms a sphere in momentum space. The Berry phase is equal to the solid angle enclosed by the loop of the polarization vector at the origin of momentum space$^{14-16}$. The other way is related to the wave polarization state vector, which spans the Poincaré sphere. The Berry phase is equal to half of the solid angle, $\Omega$, resulting in a solid angle, $\Omega/2 = \pi$, of half-integer numbers of wavelengths, and the phase mismatch is precisely compensated by the presence of Berry phase $\pi$, which leads to a 180° wave-flip. In the curved-strip cavity, the even number ($N = 116$) of antinodes corresponds to the conventional constructive interference with an integer number ($M = 58$) of wavelengths.

For linear polarization, the polarization state can be described by $|s\rangle = \frac{1}{\sqrt{2}}(|+\rangle + |−\rangle)$, where $|+\rangle$ and $|−\rangle$ are right and left circular bases. The continuous variation of the polarization orientation can be visualized as a closed loop along the equator of the Poincaré sphere (Fig. 1, left), resulting in a solid angle, $\Omega = 2\pi$. Hence, a Berry phase as large as half the solid angle, $\Omega/2 = \pi$, is generated for the right and left circular polarization bases as $|s'\rangle = \frac{1}{\sqrt{2}}(e^{i\pi}|+\rangle + e^{-i\pi}|−\rangle)$ (refs. 11–13). For optical resonances in curved-strip cavities, the trajectory of the polarization evolution on the Poincaré sphere is topologically trivial and thus does not generate any Berry phase, as illustrated in Fig. 1. The similar photon propagation trajectory and propagation constant render the curved-strip cavity a perfect reference for our study of quantifying the Berry phase.

Light ellipticity in Möbius strips

Two-photon polymerization-based direct laser writing was used to fabricate dielectric Möbius- and curved-strip microrings using the negative photoresist IP-Dip (Methods and Supplementary Fig. 2). The polymerized IP-Dip is transparent in the visible to near-infrared spectral range, and is thus suitable for supporting optical resonances in this range. Figure 2a,b presents scanning electron microscopy (SEM) images of Möbius- and curved-strip cavities with identical design parameters, $T/W = 0.33$ ($T = 0.9 \mu m$).

To understand the behaviour of light propagation and resonances in all-dielectric Möbius microrings, 3D numerical simulations based on the finite-element method were carried out (Methods). Figure 2 (bottom panels) presents the calculated mode profiles in typical Möbius and curved strips with $T/W = 0.33$ ($T = 0.9 \mu m$), respectively. The electric-field orientation of the resonant light rotates along the twisted strips, as can be seen in the magnified images of the horizontal and vertical sites of the Möbius and curved strips. In the Möbius-strip cavity, an odd number of antinodes ($N = 115$) is calculated, implying constructive interference with a half-integer mode number ($M = N/2 = 57.5$) of wavelengths. The constructive interference is off-phase in the case of half-integer numbers of wavelengths, and the phase mismatch is precisely compensated by the presence of Berry phase $\pi$, which leads to a 180° wave-flip. In the curved-strip cavity, the even number ($N = 116$) of antinodes corresponds to the conventional constructive interference with an integer number ($M = 58$) of wavelengths.

As a key approximation in an ideal Möbius strip, strip thickness $T$ is assumed to be much smaller than the wavelength of the considered light in the waveguiding medium ($\lambda/n$), so the optical field is strictly
When \( T/W = \frac{1}{2} \), the electric field tends to maintain its orientation as it propagates along the twisted cross-section. The main electric-field contribution is to rotate along the twisted strip. As a result, the main electric-field component in and perpendicular to the strip plane (Supplementary Fig. 3). The elliptical polarization state varies with \( T/W \) and is strongly affected by the cross-sectional dimension of the Möbius waveguiding geometry, \( T/W \), and the optical electric field. This leads to a variable Berry phase affecting both the eigenvalues and eigenstates of Möbius-strip cavities. For \( T/W = 1 \), the unmodified and non-rotating polarization state leads to the absence of the Berry phase, indicating a negligible Möbius-topology effect on the resonant light. Berry phase-involving constructive interferences in a Möbius strip are described further in Supplementary Note 5.

Manipulating Berry phases

The resonant modes were characterized by measuring transmission spectra using an evanescently coupled tapered nanofibre—a widely adopted approach for near-field delivery and probing of light waves (Methods, Supplementary Fig. 4 and Supplementary Note 2). The polarization states of the resonant light in the Möbius- and curved-strip microcavities were examined by tuning the input optical polarization, step by step. For the Möbius-strip cavity with \( T/W = 0.57 \), the measurement shows an elliptical polarization state (Fig. 3c). This is in sharp contrast to the linear polarization state for the Möbius-strip cavity with \( T/W = 0.33 \). The ellipticity as a function of \( T/W \) is further studied by comparing the resonant-mode offsets between Möbius- and curved-strip cavities with varying \( T/W \) ratios ranging between \( \approx 0.33 \) to 1. In this case, the optical electric field is no longer forced to rotate along the structure with a square-shaped core (Supplementary Fig. 6 and Supplementary Note 4), so the light does not undergo any non-trivial topological evolution. The resonant light projects a loop onto the Poincaré sphere away from the equator, depending on its ellipticity (Fig. 3e). With solid angle \( \Omega \) changing between 2\( \pi \) and 0, Berry phase \( \phi_B \) is generated for the right and left circular polarization bases as \( \vert s \rangle = \frac{1}{\sqrt{2}} (\vert + \rangle + e^{-i\phi_B} \vert - \rangle) \). Accordingly, by engineering the polarization ellipticity, one can develop a strategy to generate a variable Berry phase affecting both the eigenvalues and eigenstates of Möbius-strip cavities. For \( T/W = 1 \), no wavelength offsets are observed between the Möbius- and curved-strip cavities, indicating the absence of the extra phase, that is, the Berry phase. As \( T/W \) decreases, clear increasing resonant-mode offsets emerge in the resonant spectra measured for the Möbius- and curved-strip cavities, providing direct evidence of an increasing Berry phase acquired in the Möbius-strip samples.

The resonant mode offsets are well suited to tuning the Berry phase, as the ellipticity of the resonant light is particularly sensitive to \( T/W \) in that range. The Berry phase \( \phi_B \) extracted from the resonant-mode spectra is slightly lower than that derived from simulations over the whole \( T/W \) ratio range, as the measured resonant-mode offsets are not as large as those from theoretical calculations. In an ideal case, the resonant mode offset is solely determined by the presence of the Berry phase, and the Möbius- and curved-strip cavities generate an identical dynamic phase as a result of having the same size and curvature. In practical sample fabrication, a substantial curvature discrepancy exists between the Möbius- and curved-strips due to the structural-symmetry-induced inherent strain, which reduces the mode offsets for the two types of cavity. As such, a deviation between experimental and simulated phase values constantly exists in the entire investigated \( T/W \) ratio range except for \( T/W = 1 \), showing the same evolution trend of Berry phase as a function of \( T/W \).

**Discussion**

The above mainly focuses on circulating light with an optical electric field parallel to the strip plane (IP modes). However, resonant modes with an optical electric field perpendicular to the strip plane, termed ‘out-of-plane’ (OP) modes, can also be well supported for generation of the Berry phase at sufficiently large values of \( T \). Similar to IP modes, OP modes with linear and elliptical polarizations can be formed for the generation of a variable Berry phase. Simulation and experimental results for OP modes and the associated Berry phases, presented in Supplementary Figs. 8 and 9 and Supplementary Notes 6 and 7, show similar behaviour to IP modes.
such as supporting optical framed knots as information carriers. The topological invariance in the adiabatic evolution. The Möbius waveguiding structures operate in the optical wavelength range and are of micrometre size, much smaller than those investigated in previous reports using helical waveguides and other open-light-path systems. Such a miniaturized optical component is suitable for a new generation of on-chip integrable systems with excellent topological robustness for fundamental physics and practical applications. The programming of optical 'Mobiosity' as a new route to light-topology shaping has the potential to serve as a versatile knob for all-optical manipulation of both classical bits and qubits, and implies promising functionalities such as supporting optical framed knots as information carriers, and quantum logic gates in quantum computation and simulation.

Online content
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tilted orientation was carefully examined by connecting a fibre-coupled waveguide to the incident laser light, which was controlled by a fibre-based three-paddle polarimeter (PAX1000IR2, Thorlabs). Resonances with a maximized extinction ratio of $>10\,$dB were obtained by finely adjusting the coupling gap spacing. The polarization state of the primary-beam energy of 5 keV. Optical transmission measurements were conducted using an evanescently coupled tapered fibre. The optical set-up and details of preparing the tapered fibre are provided in Supplementary Note 2. A wavelength-tunable infrared laser (Tunics, Yenista) was used as the light source, with a scanning range of 1,500–1,560 nm. IP and OP excitations were provided by a local line current source at the waveguide core oscillating along the corresponding directions. The local polarization state was extracted by analysing the electric-field distributions at the field maxima point of the waveguide’s cross-section spanning from one mode antinode to node, and is presented using a projected polar plot.

Device fabrication

Pure quartz glass substrates were cleaned by immersion in acetone and isopropyl alcohol, ultrasonicated (Elasonic S, Elma Schmidbauer), and dried with 



Device characterization

For SEM imaging, the samples were sputter-coated with a thin (~8 nm) Cr layer to avoid changing and to improve contrast. The SEM images were acquired using an NVision40 system (Carl Zeiss) using a primary-beam energy of 5 keV. Optical transmission measurements were conducted using an evanescently coupled tapered fibre. The optical set-up and details of preparing the tapered fibre are provided in Supplementary Note 2. A wavelength-tunable infrared laser (Tunics 100S-HP, Yenista) was used as the light source, with a scanning range covering 1,500–1,600 nm. The transmission signal was measured using an InGaAs switchable-gain photodetector (PDA20CS-EC, Thorlabs). Resonances with a maximized extinction ratio of $>10\,$dB were obtained by finely adjusting the coupling gap spacing. The polarization state of the incident laser light was controlled by a fibre-based three-paddle polarizer. Launching of linearly polarized light with a tilted orientation was carefully examined by connecting a fibre-coupled polarimeter (PAX1000IR2, Thorlabs) at the output. Polarization mapping was carried out by adjusting the polarization angle of the input laser light in steps of 10°. The Berry phase was estimated by deriving the compensated phase value (that is, the resonant wavelength offset) for spectral matching of the resonance modes in Möbius- and curved-strip cavities with identical structural parameters.

Data availability

The main data supporting the findings of this study are available within the Supplementary Information. Additional data are available from the corresponding authors upon reasonable request.

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Author contributions

L.M., O.G.S. and J.W. conceived the study, inspired by an initial investigation with S.L. and V.M.F. J.W., S.L., C.H.L., R.T. and V.M.F. performed the theoretical calculations and analysis. S.V., L.S. and M.M.-S. fabricated the samples. S.V. and J.W. conducted the optical experiments. S.B. conducted SEM characterizations. J.W., L.M., Y.Y. and S.L. analysed the data. J.W. and L.M. wrote the manuscript. All authors discussed the results and contributed to the manuscript.

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Competing interests

The authors declare no competing interests.

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