A Machine Learning based Music Retrieval and Recommendation System

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Abstract

In this paper, we present a music retrieval and recommendation system using machine learning techniques. We propose a query by humming system for music retrieval that uses deep neural networks for note transcription and a note-based retrieval system for retrieving the correct song from the database. We evaluate our query by humming system using the standard MIREX QBSH dataset. We also propose a similar artist recommendation system which recommends similar artists based on acoustic features of the artists’ music, online text descriptions of the artists and social media data. We use supervised machine learning techniques over all our features and compare our recommendation results to those produced by a popular similar artist recommendation website.

Keywords: query by humming, similar artist recommendation, music information retrieval, machine learning

1. Introduction

Faster computational speed and increasing number of online users have resulted in a dramatic increase in music consumption. It is getting more and more difficult for the general public, especially non-experts, to find and retrieve music from the millions of songs available online. A lot of research is being done these days to find efficient music retrieval and recommendation methods. One music retrieval method that is gaining a lot of popularity these days due to its convenient usage is query by humming, which is a content-based music retrieval method that can retrieve melodies using users’ hummings as queries. This allows users to find old songs that they only remember the tune of or retrieve obscure songs heard in public places. The Music Information Retrieval (MIR) community has also been doing a lot of work on automatic recommendation systems ranging from the content-based methods to social tagging and similarity networks (Cohen and Fan, 2000; Hong et al., 2008). One of the key research topics in this area that has gained a lot of traction is automatic similar artist recommendation.

Currently, there are several musical retrieval and similar artist recommendation apps. There are apps such as Sound-Hound, MusixMatch etc, that can retrieve songs using humming as a query, and websites such as All Music Guide (AMG)\textsuperscript{1} and last.fm\textsuperscript{2} that give similar artist recommendations. However, accuracy and efficiency of these music retrieval and recommendation systems still leave a lot of room for improvement. Therefore, we are planning to create a holistic music retrieval and recommendation system using machine learning techniques.

The biggest challenges of a query by humming system include i) queries sung by users often vary from the actual melody in pitch, tempo etc. so the melodic similarity matching must be done at a more abstract level in order to get meaningful results, ii) background noise is often present in users’ queries which also makes it harder to identify the melody correctly and iii) efficient retrieval methods must be used that can search through a database and retrieve the correct melody in as little time as possible. Therefore, methods used to retrieve the melody in this case need to be robust to noise and inaccuracies in the singing or humming which is very challenging, and, for the system to be practical, the entire system should be very fast.

Therefore, we propose a supervised machine learning based method for the query-by-humming system, which can learn the common errors associated with human humming and build a model that is unaffected by these errors. For this task, we have collected humming data and transcribed them in order to train a Deep Neural Network (DNN) based Hidden Markov Model (HMM) for note transcription. This deep learning method allows us to learn the patterns present in the humming data and create a model that can detect the notes in a humming query. The proposed note transcription method is used along with a note-based retrieval method similar to Yang et al. (2010) in order to retrieve a ranked list of songs most similar to the query.

One of the biggest challenges faced by the current similar artist recommendation systems is that they perform poorly for relatively obscure artists. Therefore we are interested in using machine learning methods to build a recommendation system that can provide good similar artist recommendation even for relatively unknown artists. We propose a recommendation system that uses supervised machine learning techniques over features such as acoustics of music, the meta-data, and online texts related to the artist to find similar artists.

2. Previous Work

The main components of a QBH system consist of i) representation of the query and actual songs and ii) retrieval the songs efficiently and accurately from the database. A song or a query is mainly represented using frame-based and note-based methods. The frame-based methods use a representation of the extracted pitch to represent the query and the songs and then use some template-matching similarity measures such as DTW (Dynamic time warping) to

\textsuperscript{1}http://www.allmusic.com
\textsuperscript{2}http://www.last.fm/
measure similarity between the main songs and the query (Wang et al., 2008; Dannenberg et al., 2007). The note-based methods use the pitches as features to transcribe the notes present in a query or a song (Shih et al., 2002; Shih et al., 2003; Shifrin et al., 2002) and the notes in the query are then matched against the notes in songs using simple string matching techniques (Ghias et al., 1995; Shih et al., 2002) or linear scaling based methods (Yang et al., 2010).

In this paper, we focus on note-based methods since they are more efficient (Kharat et al., 2015; Yang et al., 2010) and there still seems to be room for improvement in accuracy in this case. These methods are often based on statistical approaches. Hidden Markov model (HMM) is one of the common methods that have been used for note transcription (Shih et al., 2002; Shih et al., 2003; Shifrin et al., 2002; Ryynänen and Klapuri, 2004). In Shih et al. (2002) and Shih et al. (2003), the note is segmented by modelling phonemes using mel-frequency cepstral coefficients, energy measures, and the derivatives of these as features, and then the average pitch of the note is found on the segmented segments, which is then used to represent the individual notes. However, this approach works well when each note is hummed using one syllable such as da or ta and is not very effective for handling a large variety of queries. The most effective of these statistical melody transcription approaches is proposed in Ryynänen and Klapuri (2004), which extracts prosodic features, that are used to train HMM-GMMs for modelling notes. Since recent studies in speech recognition field have shown that using DNN instead of GMMs in HMM significantly improves the recognition accuracy (Dahl et al., 2012), we propose to use Deep Neural Networks (DNN) with HMMs instead of simple HMM-GMM models as humming is similar to speech.

The methodology used in our artist recommendation system differs from previous work both in the source and target. We collect tons of news from mainstream news websites and calculate the co-occurrence of Bollywood artists’ names in these articles, which is a plausible profound and comprehensive way to tell the relativeness of two singers. On the other hand, related artists ought to influence each other in their musical style. Therefore, we are also extracting audio-based features to find related artists. Voice features such as Mel Frequency Cepstrum Coefficients (MFCCs) (Mermelstein, 1976) are wildly used in speech recognition and audio fingerprinting (Cano et al., 2005). Features of MFCCs include spectral flatness, tone peaks, which could represent the features and categories of the songs. In addition, musical features like loudness, pitch and brightness are also used for query of music (Wold et al., 1996). Su et al. (2013) have previously investigated piece-level features for determining the mood of a musical piece with high accuracy.

The rest of the paper is organized as follows. Section 3 describes the overall methodology, Section 4 describes the query by humming system, Section 5 describes the similar artist recommendation system, Section 6 explains the experimental setup and evaluation of the system and Section 7 summarizes the content of the paper.

3. Methodology

The overall system takes a hummed tune as an input, which is then fed to the Query by Humming (QBH) system. The QBH system uses the input to output a ranked list of songs with highest similarities to the query. The user can then either manually choose the correct song from the ranked list or use the default setting of choosing the most highly ranked song as the song to be retrieved. The retrieved song along with its metadata is then used as an input to the similar artist recommendation system, which then outputs a list of most similar artists. An overview of the overall system is given below in Figure 1.

![Figure 1: Overview of the overall music retrieval and recommendation system](image)

The Query by Humming system and similar artist recommendation system are described in more detail in sections 4 and 5 respectively.

4. Query by Humming

The Query by Humming system takes a few notes from a melody hummed or sung by the user as the query. The notes of the query is transcribed using our note transcription method and is then passed onto the retrieval system, which uses the transcribed query and the melody database, which refers to the entire list of pre-transcribed melodies or songs that can be recognized by our system, to give a ranked list of melodies that match the input query.

![Figure 2: Overview of the QBH system](image)

4.1. Note Transcription

4.1.1. Feature Extraction

As mentioned earlier, pitch is the most important characteristic of the melody. Currently, none of the pitch extrac-
tion algorithms is completely accurate. Therefore, we de-
cided to use three of the best pitch extraction algorithms
according to Molina et al. (2014) as features to improve
our systems accuracy. Those features include the pitchy-
infft (Brossier, 2006), melodia (Salamon et al., 2014) and
pyin (Mauch and Dixon, 2014) algorithms.

4.1.2. Acoustic Modelling
For this task, we propose to train notes in the range of 35-85
since this range generally covers all the notes used for hu-
man humming. We use 3-state HMM monophone models
to train each of the notes and a single-state HMM to train
the silence model.
The extracted features are then used to train the models by
using the greedy layer-wise supervised training (Dahl et al.,
2012) method, which takes the extracted features as input
and uses three hidden layers for training, which was found
to be the optimal number of layers for this task. The DNN
is trained using the Kaldi toolkit 3.

Figure 3: Overview of the acoustic modelling of the note
transcription system

4.1.3. Musicological Modelling
The musicological model controls transitions among the
note models and the rest in a manner similar to the language
model used in speech recognition.
The transition probabilities among note HMMs are de-
defined by note bi-grams, which were estimated from a
large database of MIDI files containing melodies similar to
Ryynänen and Klappuri (2004). Since key is important in de-
termining note transitions as some note sequences are more
common than others in a certain musical key, the model
first estimates the key of the musical piece. Then differ-
ent note bigrams are defined for each key. Therefore, given
the previous note i and the estimated key k, the note bi-
gram probability \( P(n=j|n=i,k) \) gives the probability
of moving from note i to note j.

4.2. Candidate Melody Retrieval
The final step is to retrieve the candidate melody repre-
seed by the hummed query. For this purpose, the melody
contour of the query is matched against those of all the
songs in the database. The melodies ranking the highest
similarity scores are presented as the candidate melodies.
The retrieval method used is similar to Yang et al. (2010).
It mainly uses note-based linear scaling (NLS) and note-
based recursive alignment (NRA). It uses the pitch and time
information of the note and recursive-alignment combined
with linear scaling to match the query with the melody.
However, instead of using absolute pitch values like in Yang
et al. (2010), we use the note transition values to match the
similarities.
The note based linear scaling algorithm basically uses dif-
ferent scale factors to stretch and contract the humming
query input. The distance between the humming and the
song is calculated by adding those between all the intervals.
The smallest distance is then used. The basic principle be-
hind the note based linear scaling method is shown using
Figures 4 and 5. The same humming query is used in both
figures with different scaling and the main melody. As it
can be seen from the figures, the scaling of the query has a
huge impact when we calculate its distance from the main
melody.

The note based linear scaling distance calculates the global
distance between humming and the main song. Note based
recursive alignment is used for the local alignment. Linear
scaling using a single value is generally not so effective be-
cause the duration of the note segments often varies greatly.
Therefore, the humming query input is generally divided
into several segments and linear scaling is used on each of
the segment to get the optimal distance between the query

\[\text{Figure 4: Principle behind NLS}\]
and the melody. Figure 6 shows the general principles of NRA.

The candidate songs are then ranked by their smallest distance with the query, with the song with the lowest distance ranked first. The retrieval method is used to generate a ranked list of top 20 songs most similar to the query.

## 5. Similar Artist Recommendation

We test the similar artist recommendation system on Bollywood artists mostly because Bollywood music provides us with a comparatively small set, which is easier to annotate and evaluate.

### 5.1. Dataset Building

Bollywood industry is a relatively small circle with a total number of 116 artists. There are three main websites that introduce and discuss Bollywood artists in both English and Hindi. They are NDTV\(^4\), The Indian Express\(^5\) and Wikipedia\(^6\). We have downloaded 3431 articles, 2622 from Indian Express and 809 from NDTV and Wikipedia. The articles are very comprehensive in the scope of the news they covered, including artists influences, collaborative efforts, gossip news, etc.

In order to evaluate our results, we need to manually build a standard related artist set for each artist. Regretfully, there is no acceptable gold standard online for Bollywood artists and the information available on AMG is very limited in recommending similar artists for lots of singers. We selected three Indian students with a strong Indian musical background as the annotators, and provided them with the full artists name list. They independently chose the similar artists for each target artist. We asked them to choose around 10 related artists for each candidate and pick the ones they all agree with in order to show a fair comparison to the baseline, Last.fm, which shows around 10 similar artists for each target artist. Last.fm\(^7\), a popular internet radio, and online music service, uses classification of metadata tags to find similar artists. Since its data is relatively open, it is one of the standards that music information retrieval work compares their results to.

### 5.2. Spectral Mean Distance of Audio Features

Bollywood music is influenced by both classical Indian music and modern western music. A particular Bollywood artist is a composer or singer with his/her own style. For example, Rahat Fateh Ali Khan is known to fuse devotional Muslim Sufi music with other styles. We propose that musical characteristics of an artist can be represented as the

\(^4\)http://www.ndtv.com
\(^5\)http://www.indianexpress.com
\(^6\)http://www.wikipedia.org
\(^7\)http://www.last.fm
aggregated average acoustic features of all his/her songs. We can then measure the similarity between two artists using spectral distance measurements. We extracted musical (Tzanetakis and Cook, 2000), psychoacoustic (Cabrera, 1999) and speech features (Eyben et al., 2010) from Bollywood songs for each artist in a spectral vector representation. Su et al. (2013) used these features successfully in categorizing musical genres and moods. The musical features include timbre, chroma, spectral flatness; psychological features include loudness, sharpness; sound features include frequency and speech characteristics. For each artist \( s_i \), the feature dimension is 865. Each entry \( v_i(k) \) is the mean value of the corresponding feature for artist \( s_i \). The distance of two artists over the acoustic feature space is calculated as follows:

\[
d(i,j) = \|v_i - v_j\| \tag{1}
\]

where \( i, j \) stand for two artists, \( d(i, j) \) is the distance of artist \( i \) and \( j \) over acoustic feature space, \( \| \cdot \| \) is the L2-norm, \( v_i \) is the audio feature vector of artist \( i \), dimension is 865.

Note that each feature in the acoustic space has been normalized by its mean and variance. Thus the closer the distance is, the more similar the styles of the songs of two artists are.

### 5.3. Co-occurrence in the texts

We extract the co-occurrence of two artists in the contexts. For two arbitrary artists, \( s_i \) and \( s_j \), the co-occurrence is computed as follows:

\[
co(i,j) = \frac{c_i^T c_j}{|c_i||c_j|} \tag{2}
\]

where \( co(i,j) \) is the co-occurrence score of artist \( i \) and \( j \). \( c_i \) is the number of times artist \( i \) occurs in each window, \( |\cdot| \) is the L1-norm. For simplicity, we set our window size to the length of each paragraph.

### 5.4. Degree of related artists

| name             | degree | rank | Listeners |
|------------------|--------|------|-----------|
| Lata Mangeshkar  | 320    | 1    | 91.4k     |
| A R Rahman       | 233    | 2    | 328.3k    |
| Kishore Kumar    | 199    | 3    | 53.1k     |
| Vijay Benedict   | 0      | 115  | 1.25k     |
| Vijay Yesudas    | 0      | 116  | 2.06k     |

Table 1: The rank of artists sorted by their degree. Listeners are the data from Last.fm

The co-occurrence score measures the closeness of two artists in the text. In this section, we propose a new feature called, degree. In Graph theory, the degree means the number of edges that are incident on the vertex. Analogous to this definition, we define the degree of an artist as the number of times that the other artists are "incident on" the artist. Given any artist as the vertex, we calculate all the times that the other artists co-occur in the same paragraph when moving the window throughout the whole articles. The degree for the artist is calculated as follows:

\[
r_i = \sum_{j \neq i, k} (c_k(i, j) > 0 ? 1 : 0) \tag{3}
\]

where \( c_k(i, j) \) indicate artist \( i \) and \( j \) co-occur in window \( k \). In our experiment, artists with the highest degree and lowest degree can be viewed from Table 1. We have cross-referenced the results with Last.fm play counts, which are shown in Table 1 Listeners column, for the artists and we have found that artists with the higher degree have larger play counts, which means they are more popular. Generally speaking, the artist with a higher degree tends to be more influential. This feature helps us to re-rank the candidate list and balance the results with more popular and lesser-known artists.

### 5.5. Learning Feature Weights

We now have three categories of features for our training system. They are co-occurrence of this artist with the target artist, degree of influence of this artist, and the spectral mean distance of the artist with target artist. We construct our training data set as follows. For the total number of 116 artists, we construct tuple sets. For artist \( s_i \), we have \( C_i \) and \( \hat{C}_i \), where \( \hat{C}_i \) means calculated candidate artists set that is related to \( s_i \), and \( C_i \) means standard candidate artists set that is related to \( s_i \). Thus, for each \( s_j \in \hat{C}_i \), if \( s_j \notin C_i \), we can build a tuple with the flag "false". Otherwise, the flag is set to "true". Each tuple contains four elements, that include three features and one flag. Once we get all the tuples, we split it into training set and testing set with the ratio 9:1. We use 10-fold validation for average performance. Since it is an unbalanced tuple set with negative tuples being dominant, we select negative tuples uniformly at random to the
The system is evaluated using mean Reciprocal Ranking (MRR): 

$$MRR = \frac{1}{|Q|} \sum_{i=1}^{Q} \left( \frac{1}{ranks_i} \right) \quad (4)$$

We initially used different feature sets and the MRR obtained using the different features is shown in Table 3. It indicates that using a combination of pitch values as features better results. We also first created a simple HMM-GMM based model and the results in Table 4 indicate that using Deep Neural Networks (DNN) with HMM improves the overall retrieval rate of the system. We have currently trained the transcription system on a relatively small dataset, and we believe that using additional training data can improve our overall transcription accuracy and the retrieval accuracy.

### 6.2. Results for Related Artist Recommendation

Once we have done the logistic regression, we can apply the trained weights to the test set. We evaluate each artist $s_i$ and calculate the related artists set $C_i$ and calculate the precision, recall and F-score.

Table 5 shows parts of our results. There are five columns. The first column is the baseline of Last.fm’s results. The other four are the results from combination of features. Section 5.4. shows that artists with higher degree contain more correlation links to other artists, which partly reflect their influences. We show artists with the highest degree and lowest degree. From Table 5, we can see that Last.fm does not work very well for artists with low degree. Actually, we can not find similar artists information for artists with low degree on the last.fm’s website. On the contrary, our method compensates this shortage. We can see that our method performs smoothly when dealing with both high degree and low degree artists and performs 40% better on average in F-measure. Actually, the sole spectral mean distance feature has already reached a pretty good precision and recall for some artists. Combined with co-occurrence features, we can see that precision and recall increased for the high degree artists whereas they did not decrease on the low degree artists. However, the co-occurrence feature alone does not perform so well. This may be due to the fact that our corpus is not large enough, so we will continue to collect data in order to improve our results in the future.

### 7. Conclusion

In this paper, we present a music retrieval and recommendation system using machine learning techniques. We propose a Deep Neural Network (DNN) based note transcription method and create a complete query by humming music retrieval system, which we test using the standard MIREX Query by humming data set. We show that the
QBH system overall shows encouraging results and can be improved with additional data. We also propose a similar artist recommendation system and experiment the system on an exhaustive list of 116 Bollywood artists and show that the recommendations based on spectral distance, co-occurrence and degree measures give better results on average for all artists compared to popular similar artist recommendation website. We plan to collect more data in the future and test the system on a larger dataset.

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| Degree | artist name | Last.fm | spectral | CO-occurrence | Spec+Co | Spec+Co+Degree |
|--------|-------------|---------|----------|---------------|---------|----------------|
| High   | Lata Mangeshkar | 0.90 0.38 0.55 | 0.72 0.33 0.46 | 1 0.08 0.15 | 0.73 0.33 0.46 | 0.72 0.33 0.46 |
|        | A R Rahman | 0.60 0.33 0.43 | 0.82 1.00 0.90 | 0.13 0.11 0.12 | 0.45 0.56 0.50 | 0.64 0.78 0.70 |
|        | Kishore Kumar | 0.44 0.33 0.38 | 0.55 0.50 0.52 | 1.00 0.33 0.50 | 0.64 0.58 0.61 | 0.55 0.50 0.52 |
|        | Sonu Nigam | 0.25 0.20 0.22 | 0.27 0.30 0.29 | 0.20 0.10 0.13 | 0.18 0.20 0.19 | 0.36 0.40 0.38 |
| Low    | Shubha Mudgal | 0.44 0.44 0.44 | 0.73 0.89 0.80 | 0 0 0 | 0.73 0.89 0.80 | 0.73 0.89 0.80 |
|        | Shibani Kashyap | 0 0 0 | 0.73 1.00 0.84 | 0 0 0 | 0.73 1.00 0.84 | 0.55 0.75 0.63 |
|        | Rajkumari | 0.33 0.13 0.19 | 0.55 0.75 0.63 | 0 1 0.22 | 0.55 0.75 0.63 | 0.55 0.75 0.63 |
| average |            | 0.25 0.14 0.17 | 0.57 0.63 0.58 | 0.31 0.06 0.10 | 0.55 0.61 0.56 | 0.53 0.60 0.55 |

Table 5: Results (precision, recall, F-score) in percentage for comparing three features performance over the last.fm results. It is calculated by 10-fold validation. Each fold iterates for 100 times in logistic regression.
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