Prominence fine structures in weakly twisted and highly twisted magnetic flux ropes

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ABSTRACT

Context. Many prominences are supported by magnetic flux ropes. One important question is how we can determine whether the flux rope is weakly-twisted or strongly-twisted.

Aims. In this paper, we attempted to check whether prominences supported by weakly-twisted and strongly-twisted flux ropes can manifest different features so that we might distinguish the two types of magnetic structures by their appearance.

Methods. We performed pseudo three-dimensional simulations of two magnetic flux ropes with different twists.

Results. We found that the resulting two prominences differ in many aspects. The prominence supported by a weakly-twisted flux rope is composed mainly of transient threads (~82.8%), forming high-speed flows inside the prominence. Its horns are evident. Conversely, the one supported by a highly-twisted flux rope consists mainly of stable quasi-stationary threads (~60.6%), including longer independently trapped threads and shorter magnetically connected threads. It is also revealed that the prominence spine deviates from the flux rope axis in the vertical direction and from the photospheric polarity inversion line projected on the solar surface, especially for the weakly-twisted magnetic flux rope.

Conclusions. The two types of prominences differ significantly in appearance. It is also suggested that a piling-up of short threads in highly-twisted flux ropes might account for the vertical-like threads in some prominences.

Key words. Sun: filaments, prominences – Sun: corona – hydrodynamics – methods: numerical

1. Introduction

Solar prominences, also known as solar filaments, are one of the most fascinating phenomena in astrophysics, which sustain a low temperature (~7000 K) plasma in the hot solar corona with a temperature of 1–2 million Kelvin. They are about 100 times denser (10¹⁰–10¹¹ cm⁻³) than their surroundings, and are believed to be supported by magnetic Lorentz force against gravity. Prominences are usually formed above polarity inversion lines (PILs), which separate positive and negative magnetic polarities. Their threads are slightly skewed from the PIL, implying that prominences are hosted by strongly sheared and/or twisted magnetic structures. Correspondingly, prominences were modeled by either magnetic sheared arcades (Kippenhahn & Schlüter 1957) or magnetic flux ropes (MFR; Kuperus & Raadu 1974). It is noted that the two magnetic configurations in two dimensions (2D) are distinct in the sense that flux ropes have the inverse polarity whereas sheared arcades have normal polarity. In three-dimensional (3D) scenarios, some sheared arcades might also have weak inverse polarity (DeVore & Antiochos 2000). In this regard, it was suggested that a magnetic configuration is classified as sheared arcades when the twisted flux is much smaller than the sheared flux (Patsourakos et al. 2020).

The most straightforward method to diagnose the magnetic structure is to measure the magnetic field of prominences based on the Zeeman effect or Hanle effect. The measurements conducted by Leroy et al. (1984) and Bommier & Leroy (1998) indicated that the majority of prominences belong to the inverse-polarity type, and much fewer belong to the normal-polarity type. Considering that the magnetic measurements of prominences are not routinely available nowadays, an indirect method was proposed by Chen et al. (2014) to distinguish between sheared arcades and flux ropes based on extreme ultraviolet (EUV) imaging observations only, without the help of magnetic measurements (see Chen et al. 2020, for a schematic). Applying this method to 571 filaments, Ouyang et al. (2017) revealed that ~89% of the filaments are supported by flux ropes, and ~11% are supported by magnetic sheared arcades.

However, all the above-mentioned methods cannot tell how strongly the coronal magnetic field is twisted around a prominence, which is crucial in determining whether the prominence might experience kink instability (Hood & Priest 1979). For this purpose, a better and widely-adopted way is to derive the coronal magnetic field surrounding a prominence via nonlinear force-free field (NLFFF) extrapolations based on the vector magnetograms on the solar surface. The NLFFF extrapolations have actually made great contributions to the understanding of the magnetic structures of prominences (Wiegelmann & Sakurai 2021). For example, Guo et al. (2010) found that an active-region prominence is partly supported by a twisted flux rope and partly by a sheared arcade; Jiang et al. (2014) constructed a twisted flux rope model for a large-scale prominence.
Regarding the magnetic twist of extrapolated flux ropes, some prominences were claimed to be supported by weakly twisted flux ropes (Jibben et al. 2016; Luna et al. 2017), and others were claimed to be supported by highly twisted flux ropes (Su et al. 2015; Guo et al. 2019; Mackay et al. 2020; Guo et al. 2021a). Guo et al. (2021a) found that the mean twist of a flux rope is proportional to its aspect ratio. Among that, the magnetic twists of some large-scale filaments can reach 3 turns (Guo et al. 2019; Guo et al. 2021a). Notably, both simulations and observations suggested that the critical twist for the kink instability depends on the flux-rope configuration (Török et al. 2004; Török & Kliem 2005; Wang et al. 2016; Liu et al. 2019). Apart from that, the gravity of the filament material can also suppress the eruption of a flux rope (Fan 2018; Fan 2020). Therefore, highly twisted flux ropes may probably exist before the eruption, in particular for large-scale quiescent prominences located in weak-field regions. The diverse results raise a concern whether the magnetic flux ropes are always weakly twisted or can be highly twisted before the eruption. The uncertainty of the extrapolated coronal magnetic configuration results from the weakness of the extrapolation method: First, the NLFFF extrapolation is an ill-posed problem (Low & Lou 1990), and the existence of inevitable magnetic tangential discontinuity can hardly be extrapolated (Low 2015). Second, there exists the 180° ambiguity in the transverse magnetic field measurements, which is crucial in determining whether the core magnetic field of the prominence is a magnetic sheared arcade or a flux rope based on the extrapolated coronal magnetic field. Furthermore, quiescent prominences are usually located in decayed active regions or quiet regions, where the transverse magnetic field is too weak to be measured precisely so far. As a result, the direct NLFFF extrapolations, such as the optimization method (Wheatland et al. 2000; Wiegelmann 2004) and the magneto-frictional method (Yang et al. 1988; Guo et al. 2016a,b), might be erroneous in modeling reasonable magnetic structures around quiescent prominences. It is noted that the uncertainty in coronal magnetic field extrapolation can be alleviated by combining coronal observations, as used in the flux-rope insertion method (van Ballegooijen 2004) or the regularized Biot-Savart laws (RBSLs; Titov et al. 2018).

On the other hand, as the building block of a prominence, cold dense threads are believed to trace the local magnetic field lines, so the thread characteristics strongly depend on their supporting magnetic configuration. Therefore, the magnetic configuration of a prominence can be reflected through the morphology and fine structures of the prominence. For example, Karpen et al. (2003) found that the prominences supported by sheared arcades are more dynamic than those supported by flux ropes. Zhou et al. (2014) found that the thread length increases with the length of its supporting magnetic dip and decreases with the dip depth (Guo et al. 2021b). Zhou et al. (2014) found that the thread length increases with the length of its supporting magnetic dip and decreases with the dip depth (Guo et al. 2021b). Therefore, we assume that the magnetic field remains unchanged during the prominence formation process, and the plasma dynamics in different magnetic flux tubes are completely independent. This approximation is valid when both the plasma β (the ratio of gas to magnetic pressures) and plasma δ (the ratio of gravity to magnetic pressure) are small (Zhou et al. 2018). Therefore, a pseudo-3D approach is equivalent to a collection of many one-dimensional (1D) hydrodynamic simulations, where the geometries of all the magnetic flux tubes are defined by the 3D force-free magnetic field. Such an approach is practical for other reasons: First, for most of the quiescent phenomena, the magnetic structure can be regarded as quasi-static on the time scale of prominence formation (Martin 1998). Second, the thermal conductivity perpendicular to the magnetic field line is about 10^12 times smaller than that parallel to the magnetic field line (Braginskii 1965), hence neighboring flux tubes can be considered as thermally isolated. The pseudo-3D approach can overcome the drawback of low resolution in 3D full magnetohydrodynamics (MHD) simulations, and has the advantage of the 3D visualization at the same time. Therefore, this method has been widely used to study prominence formation (Karpen et al. 2003; Luna et al. 2012; Guo et al. 2021b), prominence oscillation (Zhang et al. 2012; Zhang et al. 2020; Ni et al. 2022) and long-period intensity pulsations in coronal loops (Froment et al. 2017).

The 1D hydrodynamic equations, as displayed in our earlier works (Xia et al. 2011; Zhou et al. 2014; Guo et al. 2021b), are numerically solved with the Message Passing Interface Adaptive Mesh Refinement Versatile Advection Code (MPI-AMRVAC)

1 Xia et al. 2018; Keppens et al. 2020). Note that the field-aligned thermal conduction and optically-thin radiative cooling are both included in the energy equation. The code enables adaptive mesh refinement, and we use six levels of refinement with 960 base-level grids for each 1D simulation, which leads to an effective spatial resolution ranging from 3.5 to 39.1 km. With the appropriate magnetic field environment, cold material of prominences can be formed under the following models: the evaporation-condensation model (Antiochos et al. 1999; Karpen et al. 2003; Xia et al. 2011; Xia & Keppens 2016; Zhou et al. 2020), the injection model (An et al. 1988; Wang 1999), and the levitation model (Rust & Kumar 1994). Here we resort to the evaporation-condensation model, where the background heating is the same as in our previous works (Xia et al. 2011; Zhou et al. 2014).

For the purpose of pseudo-3D simulations, as stated above, we should first provide an appropriate 3D magnetic field distribution with a flux rope. Such a magnetic configuration can be realized by simulating the evolution of magnetic arcades through magnetic reconnection driven by vortex and converging flows (Xia et al. 2014b; Xia & Keppens 2016; Zhou et al. 2018; Luna et al. 2012), flux-rope emergence (Fan 2001), or by constructing theoretical models (Titov & Démoulin 1999; Titov et al. 2014).
The former two methods need higher computational cost, and are difficult to control the twist of a flux rope. Thus, we choose the third method, that is, constructing an analytical force-free Titov-Démoulin-modified (TDm) magnetic flux rope model (Titov et al. 2014, 2018). In this model, the mean twist of the magnetic field is proportional to the aspect ratio of the flux rope (Guo et al. 2021a).

The details of the TDm model construction are as follows. First, we set two magnetic charges of strength $q$ lying at a depth $d_L$ and separated by a distance $2L_q$ to construct the background potential field. Second, we set the physical parameters for two flux ropes, that is, the minor radius of the flux rope ($a$), and the major radius of the ring ($R$). With that, we can compute the toroidal electric current (Titov et al. 2014) and magnetic flux (Titov et al. 2018). Third, we construct the flux rope by the RBSSL method with the aforementioned parameters, and embed it into the background field. To quantitatively study the twisting property of the two flux ropes, we calculate the twist number ($T_g$) using Formula (12) in Berger & Prior (2006). In the two models, one has a weakly-twisted flux rope, and the other has a highly-twisted flux rope. For the low-twist flux rope model (labeled as Low-T model), $R_g = 43$ Mm, $a = 20$ Mm, $d_L = 16$ Mm, $q = 40$ T $\cdot$ Mm$^2$ and $|T_g| = 1.07$. The distance between the two footprints of the flux rope, $L_{fp}$, is about 80 Mm, and the apex height, $h_{ap}$, is about 27 Mm. For the high-twist flux rope model (labeled as High-T model), $R_g = 170$ Mm, $a = 25$ Mm, $d_L = 115$ Mm, $q = 50$ T $\cdot$ Mm$^2$ and $|T_g| = 2.64$. Correspondingly, $L_{fp} = 250$ Mm, and $h_{ap} = 55$ Mm. The mean twists are $1.07 \pm 0.20$ and $2.64 \pm 0.56$ for the two flux ropes, respectively. These quantities are in the typical range of solar prominences (Handberg-Hansen 1995, Engvold 2015). Figure 1 shows the two magnetic field models. It is noticed that the twist of the magnetic configurations in Luna et al. (2012) and DeVore et al. (2005) is about 1 turn, which is analogous to our Low-T model.

From each magnetic field model, we select 250 magnetic field lines to perform 1D hydrodynamic simulations, which are roughly uniformly distributed inside the magnetic flux rope. The localized heating is symmetrically imposed at the two footprints of each flux tube, with the amplitude $E_1 = 1.0 \times 10^{-2}$ erg cm$^{-3}$ s$^{-1}$ (Xia et al. 2011). Similar to Karpen et al. (2003), the localized heating is ramped up linearly over 860 s and maintained thereafter. Since the field-aligned gravity is not uniform and flux-tube dependent, we compute its distribution according to the field line path, that is, $g_\parallel(x) = g_0 \cdot \hat{e}_s$, where $g_0 = 274 \hat{e}_c$, $m$ s$^{-2}$, $s$ is the 1D coordinate along the field line, and $\hat{e}_s$ is the unit tangential vector along the field line. Our atmospheric model is the same as in the previous simulations (Zhou et al. 2017, Guo et al. 2021a), where the chromospheric temperature is about 6000 K, the density at the bottom is about $1.6 \times 10^9$ cm$^{-3}$, the coronal temperature is about 1 MK, and the thickness of the chromosphere is about 3 Mm. The atmospheric obtained in this way is not in thermodynamic equilibrium, therefore we relax this initial state to a state both in force and energy equilibria in about 57 min.

3. Numerical Results

3.1. Thread formation process and fine structures

Note that although the mean twist is significantly different between the two model flux ropes, both of them have three types of field lines, that is, non-dipped, single-dipped and multi-dipped field lines, with different percentages. Figure 2 depicts the temporal evolution of the temperature distributions along three types of flux tubes in each model. The first row, Figures 2a and 2b, shows the dynamic thread formation and evolution processes along the non-dipped flux tubes in Low-T and High-T models. It is seen that the flux tubes without dips experience thermal non-equilibrium cycles, similar to previous works (Karpen et al. 2001, Proment et al. 2017), forming dynamic threads moving at a high speed (Karpen et al. 2001). For the dynamic threads in the Low-T model (Fig. 2a), the period of the thread appearance is about 114.7 min, the thread lifetime is about 28.6 min, and the average velocity during the drainage is about 25.2 km s$^{-1}$, which is consistent with observations (Zirker et al. 1998, Lin et al. 2003, 2005). For that in the High-T model (Fig. 2b), the period of the thermal non-equilibrium cycle is about 378.4 min, the thread lifetime is about 194.9 min, and the average velocity is roughly 7.9 km s$^{-1}$. One can find that the period of the thermal non-equilibrium cycle increases with the flux-tube length, which is consistent with the results of Luna et al. (2012). These small dynamic threads, called “blobs” in Luna et al. (2012), are generally formed in non-dipped arcades or shallow-dipped field lines and move downward to the chromosphere, forming counter-streaming flows. The second row of Fig. 2 illustrates the evolution of temperature along single-dipped flux tubes in the two models (Figs 2c and 2d). In the Low-T model, only one thread is formed near the magnetic dip after the localized heating continues for 2.34 hr. The thread is rather stable after quick damping of short-period oscillations, growing with time as the chromospheric evaporation continues. In contrast, in the High-T model, a thread is formed slightly away from the magnetic dip at $t=0$, which then oscillates for several periods until it becomes stable at the magnetic dip. Besides, a second thread is formed at $s = 50$ Mm. This thread drains down to the footpoint, forming a
dynamic thread as depicted in Fig. [2]. The formation of a second thread is consistent with previous works (Karpen et al. 2006; Xia et al. 2011; Guo et al. 2021b), if only the field line is long. In particular, longer field lines could delay the onset of catastrophic cooling (Guo et al. 2021b). Therefore, even with the same localized heating, the formation of prominence thread supported by highly-twisted flux ropes needs more time than prominences supported by weakly-twisted flux ropes. The third row of Fig. 2 shows the evolution of the temperature along double-dipped flux tubes in the two models, and two threads are formed in each model as seen in panels (e) and (f).

With the simulation results of all the 250 flux tubes in each model at the end of simulations (t ~ 23 hr), we can compile them and construct a 3D view of each prominence. In this paper, a prominence is called filament when viewed from above, similar to the terminology in observations. Figures 5a–5c display the distribution of the formed threads in the Low-T model viewed from different perspectives. As viewed from the top, we can see in Fig. 5a that although the photospheric magnetic PIL is along the x-axis, the filament spine, as indicated by the solid blue line, is inclined to the photospheric PIL (blue dashed line) by 17.1°. The filament spine is composed of many threads, and the thread orientation deviates from the filament spine by an angle ranging from 15° to 30°. For the side view along the y-axis in panel (b), it is seen that all the threads pile up into an arch-shaped prominence, with the apex at an altitude of 16 Mm. For the end view along the z-axis in panel (c), it is seen that the apparent width is quite large, and the two legs are overlapping. For comparison, we show the distribution of the formed threads in the High-T model from different perspectives in Figs. 5d–5f. For the top view along the z-axis in panel (d), we find that the filament spine is more parallel to the photospheric PIL. Moreover, the deviation angle between the threads and the filament spine is minimal near the middle of the flux ropes, and increases toward the footpoints for both of two cases. For the side view, the prominence can approximately outline the path of the flux rope axis in the High-T model (Fig. 5e). Regarding the end view, one can see that the prominence in the High-T model is composed of many short threads compared to the prominence height (Fig. 5f), reproducing a vertical thread-like structure.

The dense and long prominences are optically thick in the EUV range, that is, partial incident light is absorbed through the photoionization of the neutral hydrogen (H I), neutral helium (He I), and singly ionized helium (He II). Therefore, we solve the radiative transfer equation to synthesize the EUV radiation images (see also Zhao et al. 2019; Zhou et al. 2020; Jenkins & Keppens 2022), which is different from our previous optically-thin modeling (Chen & Priest 2006). The solution to the radiative transfer equation (Krybicki & Lightman 1986) is as follows:

$$I_{\lambda}(\tau_s) = I_{\lambda}(0)e^{-\tau_s} + \int_{0}^{\tau_s} e^{-(\tau_s - \tau_j)}S_j(\tau_j)d\tau_j,$$

where $I_{\lambda}(\tau_j)$ is the measured specific radiation intensity at the wavelength $\lambda$, $I_{\lambda}(0)$ is the incident intensity in the background, $\tau_s$ is the total optical depth, $\tau_j$ is the local optical thickness, $S_j$ is the source function, $j_s$ is the emission coefficient and $\alpha_j$ is the absorption coefficient. Among them, the optical depth and source function are strongly dependent on the relative population of hydrogen and helium, therefore we need to calculate the ionization degree with the Saha equation. Then, the emission coefficient can be calculated according to Formula (24) in Jenkins & Keppens (2022), and the absorption coefficient can be obtained from Formula (6) in Anzer & Heinzel (2005). Finally, similar to Jenkins & Keppens (2022), assuming an incident intensity $I_{\lambda}(0)$, the transfer equation can be computed numerically, and the synthesized 171 Å images viewed from different directions are shown in Fig. 5.

For the top views, we find that the overall structure of the filament in the Low-T model looks like a rhombus, whereas in the High-T model presents stick-like morphology. Regarding the fine structures, it is seen that the filament spine is composed of right-bearing threads, which is in accord with the chirality of the filament and the helicity of the supporting flux rope. Moreover, the edge of the filament spine in the High-T model is serrated while that in the Low-T model is smoother. Comparing the side views of the two models (Figs. 5b and 5f), we find that there are no obvious legs in the prominence supported by a low-twist flux rope. That is to say, these prominences would be manifested as being nearly detached from the solar surface. However, for the prominence supported by a highly twisted flux rope, its legs almost extend down all the way to the solar surface. For the end views along the flux rope axes (Fig. 5c and 5f), the multi-dip legs appear in two models on the top of the prominence cupula, which is consistent with 3D full MHD simulations of the flux-rope prominence formation (Xia et al. 2014a; Xia & Keppens 2016; Fan et al. 2018; Fan & Liu 2019). Other than that, we also find that the horn-like structures are much more evident in the Low-T model than in the High-T model.

### 3.2. Magnetic dip and thread characteristics

High-resolution observations revealed that prominences are composed of numerous separate fine-scale threads (Lin et al. 2005), which can be divided into dynamic threads, independently trapped threads and magnetically connected threads (Guo et al. 2021b). These threads were found to move with velocities of roughly $15\pm10$ km s⁻¹ (Engvold 2004; Lin et al. 2005). The relationship between threads and magnetic dip is an important issue. Our pseudo-3D simulations provide a chance to study their relationship in detail.

As mentioned in Section 3.1 although the mean twist is 1.07 turns in the Low-T model and 2.64 turns in the High-T model, both models have non-dipped field lines, single-dipped field lines, and multi-dipped field lines. Figures 5g and 5h show the fractions of the field lines without a single dip (Fig. 5g) and with multiple dips (Fig. 5h) in the two models. One can see that whereas most field lines (78%) are non-dipped in the Low-T model, only 26.4% of the field lines are non-dipped in the High-T model. In particular, 48.4% of the field lines possess more than one dip in the High-T model. We also calculate the fractions of different types of threads, which are shown in Figs. 5i and 5j. It is found that 82.8% of the threads are dynamic threads in the Low-T model, and others (17.2%) are quasi-static threads oscillating near magnetic dips. On the other hand, 60.6% of the threads are quasi-static threads in the High-T model.

Thread length is another observational feature that can shed light on the magnetic structure of the supporting field lines of prominences (Karpen et al. 2003; Zhou et al. 2014; Guo et al. 2021b). Rather than investigating the relationship between the thread length and the parameters of the magnetic dip as done by Zhou et al. (2014), we intend to check the relationship between the thread length and the total length of the magnetic field line for simplicity. For this purpose, we select the quasi-static threads, and the thread length in the multi-dip field lines is the averaged length of multiple threads. In Figs. 5k–5l, we display the dependence of the thread length ($L_t$) on the field-line length ($L_f$). It shows that despite scattering there is a tendency that the thread length decreases with the field-line length. We divide the data points into single-dipped threads (blue) and multi-dipped threads (red), and then fit the $L_f$–$L_t$ relationships with power-law functions, $L_t = A L_f^n$, for the three groups of data, that is, single-dipped threads (blue), multi-dipped threads (red) and all threads (green). For the Low-T model in Fig. 5l, the corresponding fitting functions are $L_t = 1177.8L_f^{0.80}$, $L_t = 15432.4L_f^{1.23}$, and $L_t = 1430.83L_f^{1.08}$, respectively, where $L_t$ and $L_f$ are in units of Mm. And the corresponding Spearman correlation coefficients are -0.51, -0.50 and -0.60, respectively. Regarding the High-T model in Fig. 5k, the corresponding fitting functions are $L_t = 1417686.9L_f^{1.92}$, $L_t = 2857.02L_f^{0.87}$ and $L_t = 26932.11L_f^{1.24}$, with the correlation coefficients of -0.83, -0.79 and -0.89, respectively.

It is well known that for a vertical flux tube, the typical length of a plasma structure is the scale height, which is related to gravity. By analogy, the length of a prominence thread along a magnetic dip might be re-
related to effective gravity, which is defined as \( g_e = \int_{s} \sqrt{g \parallel(s) ds/(\Lambda \sqrt{g})} \). As demonstrated by Zhou et al. (2014), such a single parameter can reflect the magnetic dip configuration comprehensively. Figures 5– 5; reveal that the thread length decreases with the effective gravity, meaning that longer threads are likely to exist in longer and shallower magnetic dips, which is consistent with Zhou et al. (2014). The relationship between the thread length and the effective gravity \( g_e \) is fitted with a linear function. In the Low-T model, the corresponding fitting functions are \( L_e = -17.11 g_e + 22.71 \), \( L_e = -31.80 g_e + 25.97 \), and \( L_e = -24.81 g_e + 24.84 \) for the single-dipped threads, multi-dipped threads, and all threads, respectively. The corresponding correlation coefficients are -0.64, -0.92 and -0.73, respectively. In the High-T model, the fitting functions are \( L_e = -45.11 g_e + 31.54 \), \( L_e = -101.55 g_e + 53.64 \), and \( L_e = -73.69 g_e + 40.85 \) for the single-dipped threads, multi-dipped threads, and all threads, respectively. The corresponding correlation coefficients are -0.89, -0.77 and -0.86, respectively. We find that the thread length is better correlated with the effective gravity than the field-line length in the Low-T model, but it is opposite for the High-T model. The reason is that in the High-T model, magnetically-connected threads account for a significant proportion. Mutual interactions among the multiple dips along an individual field line reduce the role of the local dip geometry.

4. Discussions

4.1. Morphological differences between prominences with different twists

Magnetic twist is an important parameter of magnetic structures, describing how many turns a bunch of field lines wind around an axis (Liu et al. 2016). It plays a significant role in predicting solar eruptions and understanding the dynamics of coronal mass ejections (CMEs; Chen 2017). However, the estimate of magnetic twist is non-trivial because it relies on coronal magnetic extrapolations, which are an ill-posed boundary-value problem based on noisy vector magnetic field on the solar surface. Since prominences are usually regarded as the tracers of coronal sheared-twisted magnetic structures, their morphology might reflect the twisting properties of their magnetic structures. In this paper, we explored the morphological differences between two simulated prominences with different twists. The morphological features include (1) how many threads are quasi-static and how many threads are dynamic; (2) the thread length; and (3) whether the prominence is detached from the solar surface.

Observations indicated that some threads are quasi-static, oscillating near the equilibrium positions (Jing et al. 2003), and other threads are dynamic, moving from one polarity to the other as siphon flows (Wang 1999; Zou et al. 2016). In our simulations, both types of threads exist in the simulated prominences. In the flux rope system with a low twist, the percentage of quasi-static threads is about 17%, with the remaining 83% being dynamic threads. On the contrary, in the flux rope system with a high twist, the percentage of quasi-static threads, including independently trapped threads and magnetically connected threads, is about 61%, with the remaining 39% being dynamic threads. It is seen that the prominences supported by low-twist flux ropes are mainly composed of short-lived dynamic threads, while the prominences supported by high-twist flux ropes are mainly composed of long-lived quasi-static threads. Therefore, the counterstreamings in a weakly twisted flux rope are composed mainly of alternative unidirectional flows (Zou et al. 2017), while the counterstreamings in a highly twisted flux rope are composed mainly of oscillating threads around magnetic dip (Chen et al. 2014; Zhou et al. 2020). In fact, both types of threads exist in prominences, so the counterstreamings of prominences might be composed of both prominence longitudinal oscillations and unidirectional flows, albeit the proportion is determined by the twist of the supporting flux rope. Besides, in the prominence supported by a high-twist flux rope, there are many short magnetically connected thread pairs, that is, threads pairs connected by double-dipped field lines, which tend to present drastically decaying and decayless oscillations for one thread and the other, respectively (Zhou et al. 2017a; Zhang et al. 2017).

The thread length is also systematically different in flux ropes with different twists. First, the magnetically connected threads that exist widely in prominences supported by the high-twist flux rope are usually shorter than independently trapped threads. As a result, the vertical piling of these short threads might resemble the observed vertical-like threads in quiescent prominences (Berger et al. 2008; Mackay et al. 2010; Schmieder et al. 2010; 2014). Second, while shorter dips host shorter threads (Zhou et al. 2014), we found that magnetically connected threads tend to be much shorter. As seen from the synthesized EUV images in Fig. 3, some longer threads stand out from shorter threads, and these longer threads manifest as prominence bars. Similar to the dynamic bars (Ouyang et al. 2020), these bars do not correspond to prominence feet that extend down to the solar surface.

Observations revealed that some prominences are totally suspended in the corona, whereas others possess two or multiple legs extending down to the solar surface. Our simulations indicate that the prominence in the high-twist flux rope is nearly attached to the solar surface, but the prominence in the low-twist flux rope is somewhat detached to the solar surface. Our results might imply that those detached prominences are probably supported by low-twist flux ropes, and those attached prominences with two endpoints near the solar chromosphere are supported.
by high-twist flux ropes. The simulation results in our Low-T model are similar to those in Luna et al. (2012), whose magnetic twist is about 1 turn. In both papers, the threads are almost horizontal, and the prominences are detached from the solar surface. It might imply that there is no sharp dividing line between sheared arcades and weakly-twisted flux ropes.

When viewed along the spine direction, some prominences show horn-like structures, which are intimately related coronal cavities (Schmit et al. 2013; Schmit & Gibson 2013). Our simulations well reproduced the horn-like structures. Comparing the end views of the low-twist and high-twist flux ropes in Figs. 4c and 4f, we can find that the horns are much more evident in the Low-T model than in the High-T model. We tentatively suggest that the clearer prominence horns are a signature of less twisted magnetic field lines.

Despite all these differences, the two models reveal some common features in the synthesized prominences. For example, the deviation angle between the threads and the prominence axis ranges from 10° to 35°, which are consistent with observations (Hanaoka & Sakurai 2017). On the other hand, our simulations show that such a deviation angle increases from the middle of the prominence spine to the two endpoints, which seems not a ubiquitous feature in observations. It seems that the variation of the deviation angle depends on the magnetic configuration model, and the monotonic variation from the middle of the spine to the endpoints might be an intrinsic property of the TDm flux rope model, which has a low-twist core and a high-twist outer-shell (Guo et al. 2021a). However, it gives us a hint that we might be able to utilize the distribution of the thread deviation angle to diagnose the radial distribution of the magnetic twist in the flux rope. Since the twist profile may affect the threshold of the kink instability (Baty 2001), the distribution of the thread deviation angles can serve as an important proxy of future space weather forecasting.

4.2. Relationship between prominences and flux ropes
A statistical study indicated that whereas ∼11% of prominences are supported by sheared magnetic arcades, ∼89% are supported by flux ropes (Ouyang et al. 2017). Hence, in the majority of cases the magnetic structure of prominences is a flux rope, in particular for the quiescent prominences. However, the spatial relationship between a flux rope and a prominence is unclear (Zhou et al. 2017b), and it was generally assumed that the dense plasmas of a prominence are situated at the magnetic dips, hence are located on the underside of a flux rope (Rust & Kumar 1994).

In order to check the spatial relationship between prominences and flux ropes, we overlay the simulated prominence with the magnetic flux rope in the Low-twist model together in Fig. 6. It is noted in this figure that the prominence deviates from the flux-rope axis, but also the prominence condensations do not fully fill the lower half of the flux rope. It is revealed that in the Low-twist model, the dense plasmas of the...
prominence occupy only the lower one-fourth in size of the flux rope. Therefore, we have to be careful when taking a prominence as the tracer of a magnetic flux rope for a prominence.

Another caveat is that prominences are often claimed to be located above the magnetic polarity inversion line of the photospheric magnetogram (Mackay et al. 2010). However, according to our simulations, prominence spines are skewed from the photospheric PILs and cospatial with the coronal PILs, as shown in Fig. 7. It should be pointed out that the filament threads in our simulations are located in magnetic dips. However, the troughs of these dips correspond to the local PIL at the bottom of the flux rope in the corona, not the PIL on the photosphere. Depending on the complexity of the magnetic configuration, the coronal PILs and the photospheric PILs might be roughly cospatial or might be skewed significantly.

5. Summary

In this paper, we explored the differences of prominence fine structure characteristics in two flux ropes with different twists, one with low twist, and the other with high twist. To summarize, our simulations lead to the following results:

1. The types of threads are different in the two models, which might produce different dynamic behaviors. In the low-twist model, the majority of threads are short-lived dynamic threads (83%), forming high-speed flows inside the filament. However, for the high-twist model, quasi-stationary threads accounts for about 61%, which generally present longitudinal oscillations around the dips.

2. The characteristics of the thread length are different in two models, which might produce morphological differences. First, the piling of short magnetically connected threads that widely exist in prominences supported by high-twist flux ropes might resemble the observed vertical-like structures. Second, elongated threads in single-dipped field lines probably stand out from short magnetically connected threads, manifesting as filament barbs without feet.

3. The filament spine is not cospatial with its supporting flux rope axis and PIL in the photospheric magnetogram, especially for the low-twist flux rope model. It is found that the prominence not only deviates from the flux rope axis, but also the prominence condensations do not fully fill the lower half of the flux rope. Only the lowest one-forth radial extent of the flux rope is filled with cold plasmas in our simulations. Therefore, one has to be careful when taking a prominence as the tracer of a magnetic flux rope.

It is noted that our simulations also have some drawbacks. First, these simulations are based on the evaporation-condensation model, whereas other models of prominence formation might influence the appearance of the simulated prominence. For example, for the injection model, cold material injected from the chromosphere is likely to experience expansion, which might form elongated threads (Huang et al. 2021). Second, our simulation results strongly depend on the magnetic configuration of TDm model. In the future, we will consider the pseudo-3D model based on the NLFFF extrapolations and data-driven models from observations. Third, we ignored the effects of the prominences on the magnetic structures. However, the magnetic field might be deformed by the prominence weight when plasma δ (the ratio of the gravity to the magnetic pressure) is large enough (Zhou et al. 2018). In reality, the heating at the footpoint probably be very complex, for example, the turbulent heating (Zhou et al. 2020) or the heating related to the magnetic fields (Yang et al. 2018). However, in this paper, to emphasize the effects of the magnetic configuration, we only considered a simplified...
Fig. 5. Statistical results of magnetic dip and thread characteristics in the Low-T (left column) and High-T (right column) models. Panels (a) and (b): Fractions of different types of magnetic field lines; Panels (c) and (d): Fractions of different types of threads; Panels (e) and (f): Scatter plots of the field-line length versus the mean thread length; Panels (g) and (h): Scatter plots of the effective gravity of the dip versus the thread length.

and robust pattern (continuous and steady heating independent of the magnetic fields). Nevertheless, the above findings deepened our understanding on the relationships between prominences and their supporting magnetic structures, which provides a scientific basis for studying the magnetic structures of prominences before the eruption. We also expect that high-resolution 3D full MHD simulations in the future can reinforce our conclusions.

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Fig. 6. Simulated prominence condensations and the QSL that wraps the flux rope in the Low-T model, where the green isosurface represents the simulated prominence, the blue isosurfaces represent the flux ropes and the red lines indicate the axes of flux ropes. Panels (a) and (b) represent the top and side views, respectively.
Fig. 7. Spatial relationship between the PILs and filaments in the Low-T (panels a and c) and High-T (panels b and d) models, where the red solid lines denote the PILs, and the green isosurfaces represent the simulated filaments, which are overlaid on the magnetograms (gray scale). The first row illustrates the photospheric magnetograms, and the bottom row illustrates the coronal magnetograms at the bottom of the flux rope (10 Mm for the Low-T model and 31 Mm for the High-T model).