Magnetically tunable Mie resonance-based dielectric metamaterials

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Electromagnetic materials with tunable permeability and permittivity are highly desirable for wireless communication and radar technology. However, the tunability of electromagnetic parameters is an immense challenge for conventional materials and metamaterials. Here, we demonstrate a magnetically tunable Mie resonance-based dielectric metamaterials. The magnetically tunable property is derived from the coupling of the Mie resonance of dielectric cube and ferromagnetic precession of ferrite cuboid. Both the simulated and experimental results indicate that the effective permeability and permittivity of the metamaterial can be tuned by modifying the applied magnetic field. This mechanism offers a promising means of constructing microwave devices with large tunable ranges and considerable potential for tailoring via a metamaterial route.

Electromagnetic metamaterials with exotic physic properties have stimulated tremendous fundamental and practical interests during past decade1–3. Metamaterials are a class of materials in which subwavelength features, rather than the constituent materials, control the macroscopic electromagnetic properties4. Up to now, most of present metamaterials are constructed by using artificial metallic microstructures such as split ring resonator (SRR) or wire, whose size and periodicity are far smaller than the operating wavelengths so that the response of metamaterial to electromagnetic wave can be interpreted by using effective parameters5–10. The unusual electromagnetic properties of metamaterials originate from artificial structure rather than being inherited directly from the materials, which opens a way to design material with more freedom11–13.

Recently, Mie resonance-based metamaterials have been theoretical and experimentally studied14–18. The electromagnetic wave interaction of dielectric particles with relative high permittivity can exhibit a strong magnetic or electric resonance. From the oscillation of resulting magnetic or electric dipole, negative permeability or permittivity can be produced19. Compared to SRR and related structures, Mie resonance-based metamaterial can be expected to realize low loss and isotropic properties because it does not suffer from conductive currents and capacitance gap20. It is well known that the permeability and permittivity of the materials are key factors for the propagation of the electromagnetic wave. In order to decrease the number of parts, materials for microwave devices are required to have field dependence properties and one of the easiest ways to satisfy this need is to find materials where the parameters show magnetic DC bias dependence. However, the effective parameters cannot be tuned as a result of the settled characteristic frequency band in artificial metallic structure or Mie resonance-based metamaterials, since the size and structure of those metamaterials are confirmed.

Here, we report a magnetically tunable metamaterials based on the coupling of the Mie resonance of dielectric cube and ferromagnetic precession of ferrite cuboid. The electromagnetic properties of the metamaterials were investigated by simulations and experiments. Our results demonstrate the effective permittivity and permeability of the metamaterial can be tuned by applied magnetic field.

Results

Design and characterization of the magnetically tunable Mie resonance-based dielectric metamaterial. Figure 1a shows the schematic diagram of the magnetically tunable Mie resonance-based dielectric metamaterial. The unit cell of the metamaterial is composed of one dielectric cube and two ferrite cuboids surrounded by air. Dielectric particles support an electric and magnetic dipole response attributable to Mie resonances. The effective permittivity and permeability of an array of dielectric spherical particles embedded
in a matrix can be expressed as follows\(^2\):

\[
\varepsilon_{\text{eff}} = \varepsilon_1 \left(1 + \frac{3\varepsilon}{2F(\theta) + 2K_e} \right),
\]

\(1\)

\[
\mu_{\text{eff}} = \mu_1 \left(1 + \frac{3\varepsilon}{2F(\theta) + 2K_m} \right),
\]

\(2\)

where

\[F(\theta) = \frac{2(\sin\theta - \theta \cos\theta)}{(\theta^2 - 1)\sin\theta + \theta \cos\theta}, \quad \theta = k_0 r_0 \sqrt{\varepsilon_2 \mu_2}, \quad k_0 = 2\pi/\lambda, \quad K_e = \frac{1}{2} \varepsilon_1 \frac{r}{v}, \quad K_m = \mu_1 \frac{r}{v}, \quad v = \frac{4\pi}{3} \left(\frac{r}{p}\right)^3\]

is the volume fraction of dielectric particles, \(r_0\) and \(p\) are the particle radius and the lattice constant, respectively; \(\varepsilon_1\) and \(\mu_1\) are the permittivity and permeability of the background matrix, respectively; \(\varepsilon_2\) and \(\mu_2\) are the permittivity and permeability of the dielectric particles, respectively. From Eqs. (1) and (2), we observe that the effective permittivity \(\varepsilon_{\text{eff}}\) and permeability \(\mu_{\text{eff}}\) can be not only influenced by the permittivity \(\varepsilon_2\) and the permeability \(\mu_2\) of the dielectric particles, but also affected by the permittivity \(\varepsilon_1\) and the permeability \(\mu_1\) of the background matrix. Meanwhile, by interacting with the magnetic field of an electromagnetic wave, ferromagnetic precession can arise in ferrite under an applied magnetic field. The effective permeability of the ferrite around the frequency area of ferromagnetic resonance can be expressed as follows\(^2\):

\[
\mu_3 = 1 - \frac{F_\Gamma^2 \omega_{\text{mp}}^2}{\omega^2 - \omega_{\text{mp}}^2 - i\Gamma(\omega)\omega},
\]

\(3\)

where \(\Gamma(\omega) = \left|\omega^2(\omega_m + \omega_\mu) + \omega_\mu + \omega_m\right|/2; \omega_{\text{mp}} = \sqrt{\omega_\mu(\omega_m + \omega_m)}; \omega_m = 4\pi M_{\text{sat}}^2; \omega_\mu = \gamma H; \gamma\) is the gyromagnetic ratio; \(F = \omega_m/\omega_\mu\); \(\omega_m\) and \(\omega_\mu\) are the characteristic frequency and ferromagnetic resonance frequency of the ferrite, respectively; \(M_{\text{sat}}\) is the saturation magnetization caused by the applied magnetic field; and \(H\) is the applied magnetic field. According to Eq. (3), the permeability of the ferrite can be tuned by adjusting the applied magnetic field. Because ferrite is one of the two important parts in this metamaterial, the effective permeability of the metamaterial can be influenced by the permeability of the ferrite cuboids, which means that the effective permeability of the metamaterial can be tuned by adjusting the applied magnetic field.

To simplify fabrication, cubes rather than spheres were used as the dielectric particles to prepare the metamaterial.

In order to understand the influence of applied magnetic field on the electromagnetic properties of the metamaterial, the dynamic magnetic field distributions of the unit cell were simulated. Figure 1b shows the magnetic field distributions for the unit cell with or without applied magnetic filed. Four maps with different phase (50, 140, 230 and 320 degrees) are chosen to indicate the dynamic changes of magnetic field distributions in the unit cell. For the unit cell without applied magnetic field, the dielectric cube plays a key role in interacting with electromagnetic wave, and the ferrite cuboids do not interacts with electromagnetic wave due to they have not been magnetized. At a certain frequency (Mie resonance frequency, 11.37 GHz), the magnetic field distributions in the xy-plane (the upper four maps in Fig. 1b) show a typical magnetic Mie-resonance mode. First, the magnetic fields are mainly localized in the cubes at 140 degrees along the z direction of the linearly polarized displacement currents at 140 degrees is opposite to that at 320 degrees along the z axis, which exhibits a magnetic dipole characteristic. Ferrite can be magnetized in presence of a certain external magnetic field. When a bias magnetic field (1500 Oe) is applied along z direction, the ferromagnetic precession takes place in the ferrite cuboids by interacting with the electromagnetic wave, which could influence the Mie resonance of the dielectric cube. The magnetic field distributions at 11.60 GHz for...
the unit cell with applied magnetic field are shown in the lower four maps of Fig. 1b. The magnetic field distributions at 140 and 320 degrees for the unit cell with applied magnetic field are the same as that for the unit cell without applied magnetic field. However, at 50 and 230 degrees, the magnetic field distributions for the unit cell with and without applied magnetic field are much different. According to the dynamic simulation, when a bias magnetic field is applied along the direction, the linearly polarized displacement currents in dielectric cube rotate clockwise and that in ferrite cuboids rotate anticlockwise. At 140 and 320 degrees, the behavior of the displacement currents exhibits a magnetic dipole characteristic. At 50 and 230 degrees, the magnetic field distributions in ferrite cuboids show a vortical pattern, which exhibits an electric dipole characteristic. On the basis of the analysis of the magnetic field distributions for the unit cell with or without applied magnetic field, one can predict that the applied magnetic field not only influences the permeability of the metamaterial, but also affects the permittivity of the metamaterial.

Numerical simulations. Figure 2a shows the simulated transmission spectra for the unit cell of the metamaterial under a series of applied magnetic fields \( H \). A transmission dip appears at 11.37 GHz in the absence of an applied magnetic field, which corresponds to the magnetic Mie-resonance. When a magnetic field of \( H = 500 \text{ Oe} \) is applied, one can see that two transmission dips appear at 11.24 GHz and 11.48 GHz, respectively. This indicates that the electromagnetic properties of the metamaterial can be affected by the applied magnetic field. When \( H \) is increased from 500 Oe to 2000 Oe, two transmission dips move to higher frequency region, which exhibits a magnetically tunable behavior. When \( H \) is increased to 2500 Oe, the third transmission dip appears at 8.29 GHz, corresponding to the ferromagnetic resonance of the ferrite cuboids. The effective permittivity and permeability of the unit cell of the metamaterial under the same series of applied magnetic fields \( H \) was extracted from the simulated scattering parameters using a well-developed retrieval algorithm. Figure 2b shows the dependence of the calculated effective permeability on frequency. For the unit cell without applied magnetic field, one remarkable Lorentz-type dispersion occurs in the range of 11–12 GHz. When a certain magnetic field is applied, instead of one dispersion, two or three frequency dispersions appear in the range of 11–12 GHz, which also exhibit magnetic resonance characteristic. The resonance frequency increases as \( H \) increases, consistent with the behavior observed in Fig. 2a. In addition, between the magnetic resonance frequency and the magnetic plasma frequency, the value of the effective permittivity is negative. This characteristic makes this metamaterial suitable for applications in negative refractive index materials. Figure 2c shows the dependence of the calculated effective permeability on frequency. Corresponding to each Lorentz-type dispersion for the effective permeability shown in Fig. 2b, a concurrent anti-resonance state of the effective permittivity appears due to the periodicity effect. Besides that, the electric resonance frequency increases as \( H \) increases. From the above analysis, both the effective permittivity and permeability of the metamaterial can be tuned by applied magnetic field.

Microwave measurement system. To confirm the results of the above simulations, experimental investigations of the electromagnetic properties of this metamaterial were conducted. The photograph of the microwave measurement system and the metamaterial are shown in Fig. 3. The upper and lower metal plates form the planar waveguide, which restrict the polarization of the electric field to lie uniformly along the \( z \) direction and further restrict propagation to the \( x-y \) plane. Two horn antennas connected to the output and input ports of the vector network analyzer (Agilent ENA5071C) are installed at both ends of planar waveguide (between the upper and lower metallic plates) as the waveguide adapter to excite and receive a plane wave (8–12 GHz). The sample is placed between two horn antennas. The propagation of the incident electromagnetic wave is along the \( y \) axis, and the electric field and magnetic field are along the \( z \) and \( x \) axes, respectively. The bias magnetic field is generated by an electromagnet in the \( z \) direction
and can be tuned by adjusting the input current. A teslameter is used to detect the magnetic field. The inset shows a photograph of the metamaterial and the horn antenna.

**Experimental results.** Figure 4a presents the experimental transmission spectra for the metamaterial under a series of applied magnetic fields $H$. First, a transmission dip induced by magnetic Mie-resonance of dielectric cube occurs in the transmission spectrum for the metamaterial without applied magnetic field. Second, when a certain magnetic field is applied in the $z$ direction, two transmission dips appear in the range of 11–12 GHz. The resonance frequency of the transmission dip increases as $H$ increases, which exhibits a magnetically tunable behavior. Third, when $H$ is increased from 2500 Oe to 2600 Oe, the third transmission dip induced by ferromagnetic resonance of the ferrite cuboids appear in the range of 11–12 GHz. When $H = 0$, the ferrite cuboids are not magnetized and almost have no effect on the magnetic field distributions of the unit cells, as shown in the upper four maps in Fig. 1b. The typical magnetic Mie-resonance is induced by the dielectric cube, which results in one transmission dip appeared in the spectra. The ferrite cuboids will be magnetized when $H > 0$. By interacting with the electromagnetic wave, the ferromagnetic precession takes place in the ferrite cuboids. As shown in the lower four maps in Fig. 1b, the magnetic Mie-resonance in the dielectric cube is influenced by the ferromagnetic precession. Hence, two transmission dips appear in the transmission spectra. The ferromagnetic precession in the ferrite cuboids will enhance as $H$ increases. As a result, the resonance frequency of the transmission dip increases as $H$ increases.

The real parts of the effective permeabilities retrieved from the experimental scattering parameters under the same series of applied magnetic fields $H$. The effective permittivity shows the anti-resonance state. The electric resonance frequency increases as $H$ increases, thus, magnetically tunable behavior is demonstrated. From the analysis presented above, it is evident that the behavior of the experimental data is in good agreement with that of the simulated data.

**Discussion**

We experimentally and numerically demonstrated a magnetically tunable Mie resonance-based dielectric metamaterials. The tunable property is attributable to the coupling of the Mie resonance of dielectric cube and ferromagnetic precession of ferrite cuboid. When a certain magnetic field is applied, two or three resonance frequency dispersions appear in the range of 8–12 GHz, which indicates two or three peak values can be obtained. In particular, both the effective permittivity and permeability of the metamaterial can be tuned by adjusting the applied magnetic field. This work provides a new way to fabricate the tunable metamaterials, which has greater potential for wireless communication and radar technology.

**Methods**

**Sample fabrication.** The dielectric material chosen for this work was Barium Strontium Titanate (BST) ceramic. BST cubes were cut to dimensions of $2 \times 2 \times 2$ mm$^3$. The relative permittivity and dielectric loss are 120 and 0.015, respectively. The ferrite material chosen for this work was yttrium iron garnet (YIG) ferrite. YIG cuboids were cut to dimensions of $2 \times 2 \times 1$ mm$^3$. The saturation magnetization $4\pi M_s$, linewidth $\Delta H$, and relative permittivity $\varepsilon_r$ of the YIG rods were 1950 Gs, 10 Oe, and 14.5, respectively, and the same values were used in the simulations. The unit cell of the metamaterial is composed of one dielectric cube and two ferrite cuboids. Two ferrite cuboids were bonded with both ends of the dielectric cube. The sample was fabricated by inserting the dielectric cubes and ferrite cuboids into a Teflon substrate, as shown as an inset in Fig. 3. The distance between the dielectric cubes in the $x$ direction is the same as that in the $z$ direction (5 mm).

**Simulations.** The dimensions of the unit cell were $5 \times 5 \times 5$ mm$^3$. All the parameters of the dielectric cube and ferrite cuboid were the same as those in the experiments. A plane wave was assumed for the incident electromagnetic field, with polarization conditions corresponding to an electric field along the $x$ axis and a magnetic field along the $y$ axis. The bias magnetic field was applied in the $z$ direction. Numerical predictions of the transmission spectra were calculated using the commercial time-domain package CST Microwave Studio TM.
Figure 4 | Experimental results of the magnetically tunable Mie resonance-based dielectric metamaterial. (a) Experimental transmission spectra for the metamaterial under a series of applied magnetic fields \( H \). Real parts of the effective (b) permeabilities and (c) permittivities retrieved from the experimental scattering parameters under a series of applied magnetic fields \( H \).

**Microwave measurements.** The sample was placed between two horn waveguides connected to an HP 8720ES network analyzer, as shown in Fig. 3. The propagation of the incident electromagnetic wave was along the \( y \) axis, and the electric field and magnetic field were along the \( x \) and \( z \) axes, respectively. The bias magnetic field provided by the electromagnets was applied in the \( z \) direction.

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**Author contributions**

K.B. conceived the idea and designed experiments. K.B., Y.S.G. and X.M.L. performed the experiments. K.B., Q.Z. and M.L. and J.H.X. developed the post-processing treatments of the experimental data. K.B. and Y.S.G. carried out numerical calculations and figures. K.B. and J.Z. wrote the paper. All authors contributed to scientific discussion and critical revision of the article.
Additional information

Competing financial interests: The authors declare no competing financial interests.

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