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Investigating the Interaction between Persistent Slip Bands and Surface Hard Coatings via Crystal Plasticity Simulations

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Abstract: Fatigue cracks often initiate from the surface extrusion/INTRUSIONS formed due to the operation of persistent slip bands (PSBs). Suppression of these surface topographical features by hard surface coatings can significantly extend fatigue lives under lower stress amplitudes (i.e., high cycle fatigue), while cracks initiate early in the coating or in the coating–substrate interface under higher stress amplitudes (i.e., low cycle fatigue), deteriorating the fatigue performance. However, both beneficial and detrimental effects of the coatings appear to be affected by the coating–substrate material combination and coating thickness. A quantitative understanding of the role of these factors in the fatigue performance of materials is still lacking. In this study, crystal plasticity simulations were employed to elucidate the dependence of the coating’s effects on two factors—i.e., the coating thickness and loading amplitudes. The results revealed that the thicker coatings more effectively suppress the operation of the PSBs, but generate higher tensile and shear stresses, normal and parallel to the interfaces, respectively, promoting interfacial delamination. The tensile stresses parallel to the interface within the coating, which favors coating fracture, are not sensitive to the coating thickness.

Keywords: crystal plasticity simulations; persistent slip band; surface hard coating; fatigue crack initiation

1. Introduction

Fatigue cracks for many metals often initiate from surface markings (i.e., intrusions and extrusions) formed due to cyclic slip localization [1,2]. This localized slip activity is associated with permanent changes in the microstructure of the material developed during the cyclic loading, and the slip markings can re-emerge at the same locations upon reapplication of the load even after surface polishing [3]. Due to their persistent nature, these surface markings are commonly referred to as persistent slip markings (PSMs), and the localized deformation volume is referred to as persistent slip bands (PSBs). Cyclic plastic deformation in the PSBs is typically accommodated by the motion of dislocations on the primary slip system [4–6].

For FCC materials, these dislocations have the same Burgers vectors and form very organized bundles known as veins (see Figure 1a). When these bundles collapse along the primary slip direction, PSBs are formed [7]. A typical dislocation microstructure (i.e., the ladder structure) of the PSBs constitutes regularly spaced dislocation walls separating dislocation channels, in which screw “runner”
dislocation propagates in a to-and-fro manner. The width of the dislocation channels within PSBs are on the order of 1 μm and is significantly larger than that of the one between dislocation veins. The cyclic plastic deformation therefore localizes at the PSBs [4].

![Image of PSB and PSM](image)

**Figure 1.** (a) A schematic illustration of a persistent slip band (PSB), vein structure, specimen surface, and the surface persistent slip marking (PSM). (b) The cyclic stress–strain curve of single-crystal Cu [8].

PSBs typically form within a specific range of resolved plastic shear strain amplitude of \( \Delta \gamma_{pl}/2 \approx 0.0001–0.01 \), within which the volume fraction of the PSBs linearly varies from 0% to 100%. The precise values of this range are also material-dependent. This behavior for single-crystal Cu is shown by the cyclic stress–strain curve obtained by Mughrabi [8] (see Figure 1b). Accordingly, the plastic strain amplitude within the PSB is constant at around 1% [9]. In addition, the width of the PSBs is slightly material-dependent but generally invariant with respect to the loading amplitude. As a result, the change in loading amplitude only alters the PSB density—i.e., the higher the loading amplitude is, the higher the PSB density becomes [10].

In polycrystalline metals, the location of the PSBs may shift from the surface to subsurface under very low stress or strain amplitudes (i.e., in the very high cycle fatigue regime) owing to the absence of global plasticity and the dominance of the subsurface, localized plastic deformations due to the elastic incompatibility among grains or between grains and defects [10]. Thus, the corresponding PSB–grain boundary interaction may lead to subsurface fatigue crack initiation [11]. Nevertheless, the PSM-induced surface crack initiation is still the governing mechanism in the low cycle fatigue (LCF) and high cycles fatigue (HCF) regimes encountered in many engineering applications [12–14]. Therefore, any surface treatments that act to suppress or interfere with the formation and/or operation of the PSBs may delay the initiation of fatigue cracks and substantially extend fatigue life. Well-known methods in this regard include intermittent surface repolishing, shot/sand surface peening, and surface hard coatings [3,15–19].

Surface repolishing aims to completely remove the PSMs—together with any other roughness created due to cyclic loading—at appropriate intervals mid-service, eliminating any stress concentrations (even crack embryos). Fatigue life had been shown to be extended almost indefinitely using this method, as long as sufficient serviceable material remained [15]. However, this method, due to its subtractive nature, is not suitable for part surfaces that require tight tolerances. Shot/sand peening, on the other hand, is performed prior to service and induces plastic deformation on the surface layer driven by the impact of shot or sand particles, which leaves a compressive residual stress and a refined microstructure on the surface [16,18]. However, this method results in a relatively rough surface finish and is not suitable for mating surfaces. Lastly, surface hard coatings can circumvent some disadvantages of the other methods because they are generally very thin (a few hundred nm to a μm) and create a smooth surface [19].
There are extensive works focused on examining the effect of various types of coatings—including metallic mono-/multi-layers, ceramic, metallic glass, diamond-like carbon—on the fatigue resistance of metallic specimens [17,20–26]. It has been generally observed that the coatings can improve the HCF performance of the test specimens, while they are often detrimental to the LCF performance. In the LCF regime, higher loading amplitudes tend to induce fracture within the coatings and/or lead to delamination at the coating–substrate interfaces. The precise effect of coatings on the fatigue resistance of a material greatly depends on several factors, including the coating–substrate material combination, mechanical properties and thickness of the coating, and the binding and shear strengths of the coating–substrate interface, etc. [17,19,27]. However, due to the time-intensive nature of the fatigue data generation, systemic evaluations of the influence of the aforementioned factors are still lacking.

Using crystal plasticity (CP) simulations, we aim to elucidate the effect of the coating thickness and the applied cyclic plastic strain amplitude on several characteristics of PSB–coating interaction that tend to influence the fatigue performance of coated materials. These characteristics include (1) the suppressive effects of coatings on the operation of PSBs, (2) the normal stress developed in the coating layer along the loading direction, (3) the interfacial normal stress developed perpendicular to the interface, and (4) the interfacial shear stress developed parallel to the interface. The first characteristic retards, while the rest accelerate, the initiation of fatigue cracks in the substrate. This work by no means attempts to perform direct CP simulations of fatigue failure of coated metallic materials. Instead, it focuses on the interaction between the coating and the PSBs under different loading amplitudes and aspires to generate an understanding that may benefit the geometrical design and material selection of the coatings. Indeed, cyclic damage (in the forms of dislocations and vacancy) accumulates during each cycle via cyclic plasticity and, upon reaching a critical level, leads to the initiation of fatigue cracks [28,29]. The surface coatings’ suppression of the plastic deformation per cycle is therefore indicative of the coatings’ beneficial effects on a part’s overall fatigue resistance. As such, instead of simulating the accumulation of cyclic damage over the entire fatigue life, this work only considers the loading portion of a single cyclic loading period after the PSBs has formed.

2. Computational Methods

CP simulations were performed using the Düsseldorf advanced material simulation kit (DAMASK) developed by the Max-Planck-Institut für Eisenforschung [30]. Spectral solver based on fast Fourier transform (FFT) implemented in the Portable, Extensible Toolkit for Scientific Computation (PETSc) was utilized to solve for the displacement field [31,32]. The simulation model is composed of substrates made of a single crystalline austenitic stainless steel (SS) 316 and physical vapor-deposited (PVD) thin Cr coatings. Prior literature has indicated that the common PVD Cr coatings are nanocrystalline and exhibit isotropic mechanical behavior [19].

2.1. Model Setup

Figure 2 illustrates the geometries of the simulation model. To investigate the characteristics of the interaction between PSBs and surface coatings, only the tensile loading portion of one fatigue cycle is applied. The intended boundary conditions (BCs) on the lateral coating surfaces are free—i.e., the surface tractions are zero. A rate-controlled uniaxial tension was applied by enforcing only the \( F_{zz} \) component of the deformation gradient rate tensor, while ensuring that \( \sigma_{xx} = 0 \) and \( \sigma_{yy} = 0 \). Since this work employed the spectral solver implemented in PETSc, which imposed a full periodic BC on the computational cells [30], the presence of free surfaces was mimicked by adding two soft \( \approx 1-\mu m \) thick buffers layers on both sides of the sample (see Figure 2a), which is similar to the approach by [4,33,34]. A strong contrast in elastic moduli and strengths existed between the buffer layers and the samples (the elastic constants were at least one order of magnitude lower and the strengths were at least three orders of magnitudes lower for the buffer layer). The effective BCs are therefore free, periodic, and periodic in the x-, y-, and z-directions, respectively.
To conserve computational resources, the y-dimension of the simulation cells was minimized and kept constant at ~0.2 μm. Thus, the models were thin slab-shaped. The width of the substrate along the x-direction was also kept constant at ~34 μm. The PSBs were modeled to be 45° off the loading axis (z) and to have a constant thickness of \( t_{PSB} = 1 \) μm in accordance with direct experimental observations in the open literature. Indeed, for metallic materials such as Cu, Ni, and SS 316, the thickness of the PSBs was ~1 μm [12,35]. Constrained by the periodic BC, the height of the models along the z-direction was dictated by the thickness (\( t_{PSB} \)) of and spacing (\( d_{PSB} \)) between the PSBs—i.e., \( h = \sqrt{2} (t_{PSB} + d_{PSB}) \). The spacing \( d_{PSB} \) varied between 1 and 8 μm, which corresponds to a PSB volume fraction of 50%~11%, and an overall shear plastic strain range of approximately \( \Delta \gamma_{pl} = 0.01~0.002 \) assuming a 0.01 plastic strain amplitude in the PSBs. Three different coating thicknesses (\( t_{coat} \)), namely 0.5, 1.0, and 2.0 μm, were considered here. These parameters of the models are listed in Table 1.

Table 1. Design of simulations performed in the current study. The meaning of \( t_{PSB} \) and \( d_{PSB} \) are shown in Figure 2b.

| \( t_{PSB} \) (μm) | \( d_{PSB} \) (μm) |
|-------------------|-------------------|
| 0.5               | 1, 2, 4, 8        |
| 1                 | 1, 2, 4, 8        |
| 2                 | 1, 2, 4, 8        |

Both isotropic and anisotropic plastic flow rules have been utilized in the models. The buffer layers and the coatings were treated by isotropic plasticity. This assumption is sound since the buffer layers only have marginal resistance to deformation and the nanocrystalline Cr coatings exhibit isotropic mechanical behavior. Correspondingly, the plastic flow rule is written as [30]
\[
\dot{\gamma}_p = \dot{\gamma}_0 \left( \frac{\sqrt{3J_2}}{M\xi} \right)^n,
\]

where \( \dot{\gamma}_p \) is the plastic shear strain rate, \( \dot{\gamma}_0 \) is a reference strain rate, \( n \) is the stress exponent, \( J_2 \) is the second invariant of the deviatoric stress tensor, and \( M \) is the Taylor factor. The \( \xi \) term in the denominator is the resistance to plastic flow. The rate of \( \xi \) is given as

\[
\dot{\xi} = \dot{\gamma}_p h_0 \left| 1 - \frac{\xi}{\xi_\infty} \right|^n \text{sgn} \left( 1 - \frac{\xi}{\xi_\infty} \right),
\]

where \( \dot{\gamma}_p \) is the plastic shear strain rate, \( h_0 \) is the strain hardening coefficient, \( \xi_\infty \) is the saturation resistance to plastic flow, and \( a \) is a material-dependent exponent.

Anisotropic plasticity was used for the substrate (including both the matrix and the PSBs) and a phenomenological hardening law was used. The flow rule is written as

\[
\dot{\gamma}_p^\alpha = \dot{\gamma}_0^\alpha \left| \frac{\tau^\alpha}{\xi^\alpha} \right|^n \text{sgn}(\tau^\alpha),
\]

where \( \tau^\alpha \) is the resolved shear stress on the slip system \( \alpha \), \( \xi^\alpha \) is the slip resistance on the slip system, \( \dot{\gamma}_0^\alpha \) is the reference strain rate, and \( n \) is the stress exponent. Since only the loading portion of a cyclic loading period was modeled, the back-stress term—which is necessary to capture the kinematic hardening effect in cyclic loading—is not included in the present study. The rate form of the resistance \( \xi^\alpha \) is given as

\[
\dot{\xi}^\alpha = h_0^{\delta-a} \sum_{\alpha'} N_{\alpha} \left| \dot{\gamma}^\alpha' \right| \left( 1 - \frac{\xi^\alpha'}{\xi_\infty} \right)^n \text{sgn} \left( 1 - \frac{\xi^\alpha'}{\xi_\infty} \right) \mu_{\alpha\alpha'},
\]

where \( \dot{\gamma}^\alpha' \) is shear strain rate on the slip system \( \alpha' \), \( \xi_\infty \) is the resistance saturation value, \( h_0^{\delta-a} \) is the slip hardening matrix (including both self- and latent hardening), and \( a \) is a material-dependent exponent.

The elastic and plastic flow constants used for the SS 316, PSB, coatings, and buffer layers are summarized in Tables 2 and 3. The stress–strain behaviors produced by the elastic and plastic constants are shown in Figure 3. The elastic constants of both the Cr coating and the SS 316 substrate (including both the PSBs and the matrix) were obtained from the open literature [36–38]. To obtain the plastic flow constants of SS 316, the stress–strain response of a “virtual single crystal”—which was an average of many tensile tests (>50) on single crystals of randomized orientations under the isostress assumption—was fitted to an experimental curve [39–41]. This technique, also referred to as the “material point” simulation, is a standardized practice to establish flow constants for crystal plasticity simulations [30,42,43].

**Table 2.** Anisotropic elastic and plastic material constants used for SS316 substrate (including PSB).

| Material     | \( C_{11} \) (GPa) | \( C_{12} \) (GPa) | \( C_{44} \) (GPa) | \( \dot{\gamma}_0 \) (1/sec) | \( n \) | \( \xi_0 \) (MPa) | \( \xi_\infty \) (MPa) | \( a \) | \( h_0 \) (MPa) |
|--------------|---------------------|---------------------|---------------------|-------------------------------|--------|----------------|-------------------|--------|---------------|
| SS 316 matrix| 207.0               | 133.0               | 117.0               | 0.001                         | 20.0   | 115.0          | 430.0             | 2.25   | 50.0          |
| PSB primary  | 207.0               | 133.0               | 117.0               | 0.001                         | 50.0   | 40.0           | 400.0             | 2.25   | 50.0          |

1 These values are for the primary slip system in the PSB. The slip activities in the secondary slip systems were suppressed by using much higher slip resistances (at least 1000 times higher).
PSBs within the substrate were modeled as different materials with identical elastic constants and crystallographic orientations but lower shear resistances (~100 MPa in the PSBs compared to ~300 MPa in the matrix) on the primary slip system. As discussed in the introduction, due to the wider dislocation channels within the PSB compared to the matrix, the PSBs have substantially lower critical resolved shear stress (CRSS). The applied overall strains are therefore localized within the PSBs. For pure Cu, Ni, and Ag, the respective CRSSs are ~30, 50, and 20 MPa [44]. As for SS316, the CRSS of PSBs is not known to the authors’ best knowledge and must be assumed. Considering the solid solution strengthening effect in SS316, the highest known CRSSs among the three aforementioned elemental metals, i.e., 50 MPa of Ni, was used. Assuming a Schmid factor of 0.5 (which applies for the current model geometries), the corresponding tensile yield strength is 100 MPa. As will be shown in Section 3, this choice of the CRSS appears to be sufficient to capture the strain localization within the PSBs. The slip activity on the secondary systems was completely suppressed by applying much higher critical resolved shear stresses (~40 GPa). The plastic flow constants of the coating and the buffer layer were calibrated so that they reproduce yield strengths of 750 and ~0 MPa, respectively.

Note that the crystallographic orientation of the substrate must be defined carefully, so that the primary slip system in the PSB experiences maximum shear stress under the tensile loading applied (see Figure 2b). In other words, the primary slip direction and slip plane should both be 45° off the loading axis. A cubic grid with the characteristic size ~0.09 × ~0.09 × ~0.09 µm has been chosen for all the models, leading to 2 Fourier points (FPs) along the y-direction, 400 to 440 (FP) along the x-direction, and 30 to 135 (FP) along the z-direction. The one-FP per voxel configuration is comparable to the one-integration point, C3D8R finite element type (according to ABAQUS), which was emulated in the model setup by DAMASK [45].

2.2. Post-Processing

The results were visualized using the open-source software package Paraview [46]. In all of the visualizations, the buffer layers have been removed to avoid any confusion. All the results visualized correspond to a specific point in the loading history, i.e., when the average shear strain in the primary
3. Results and Discussion

The results of the simulations were analyzed with respect to four characteristics of the coating–PSB interaction—i.e., (1) the suppressive effects of coatings on the operation of PSBs, (2) the normal stress developed in the coating layer along the loading direction, (3) the interfacial normal stress developed perpendicular to the interface, and (4) the interfacial shear stress developed parallel to the interface. For instance, typical results, including the distributions of shear strain, as well as shear and normal stresses of three selected simulations, are shown in Figure 4 for three cases: (a) \( t_{\text{coat}} = 0.5 \, \mu m, \, d_{\text{PSB}} = 1 \, \mu m, \, \Delta \gamma_{\text{pl}} = 0.01 \), (b) \( t_{\text{coat}} = 0.5 \, \mu m, \, d_{\text{PSB}} = 8 \, \mu m, \, \Delta \gamma_{\text{pl}} = 0.002 \), and (c) \( t_{\text{coat}} = 2 \, \mu m, \, d_{\text{PSB}} = 1 \, \mu m, \, \Delta \gamma_{\text{pl}} = 0.01 \), respectively. Note that the \( d_{\text{PSB}} \) and \( \Delta \gamma_{\text{pl}} \) parameters are coupled, as discussed in the previous section. Apparently, all these characteristics appear to be influenced by both the coating thickness and overall loading amplitude (reflected in the density of PSBs). In what follows, we analyze and discuss these influences from the four aforementioned aspects.

![Figure 4. Contour plots of shear strains within the PSBs, as well as normal and shear stresses near the coating–substrate interfaces (marked using the black dashed lines) for four cases of simulations: (a) \( t_{\text{coat}} = 0.5 \, \mu m, \, d_{\text{PSB}} = 1 \, \mu m, \, \Delta \gamma_{\text{pl}} = 0.01 \), (b) \( t_{\text{coat}} = 0.5 \, \mu m, \, d_{\text{PSB}} = 8 \, \mu m, \, \Delta \gamma_{\text{pl}} = 0.002 \), and (c) \( t_{\text{coat}} = 2 \, \mu m, \, d_{\text{PSB}} = 1 \, \mu m, \, \Delta \gamma_{\text{pl}} = 0.01 \).](image)

3.1. Suppressive Effects of the Coating on the Operation of PSBs (Distribution of Plastic Shear Strain in the PSBs)

Comparing the first column of Figure 4a,c, it is apparent that the thicker coating (\( t_{\text{coat}} = 2 \, \mu m \)) inhibited the slip activities (\( \gamma_{\text{primary}} \)) within the PSB, especially at locations near the coating–substrate interfaces. As expected, this suppression effect was attenuated with the increase in the strain amplitude applied (compare Figure 4a,b, which represented higher and lower applied strain amplitudes, respectively). To quantitatively compare the suppressive effect of the coatings, the plastic shear strain on the primary slip system within the PSBs were plotted in Figure 5 as a function of the distance from the coating–substrate interface along the x-direction. The plots were generated using the binning analysis, described in Section 2.2. Each panel of the figure corresponds to a different PSB spacing (\( d_{\text{PSB}} \)) and, accordingly, a different applied plastic strain range (\( \Delta \gamma_{\text{pl}} \)). The plots were obtained at the point of loading history which corresponds to an average of ~1% plastic shear strain over the entire PSBs.
Figure 5. Distribution of shear strain along x on the primary slip system within the PSBs for various PSB spacings and equivalent applied plastic strain ranges: (a) \(d_{PSB} = 1 \ \mu m\) and \(\Delta \gamma_{pl} = 0.01\), (b) \(d_{PSB} = 2 \ \mu m\) and \(\Delta \gamma_{pl} = 0.007\), (c) \(d_{PSB} = 4 \ \mu m\) and \(\Delta \gamma_{pl} = 0.004\), and (d) \(d_{PSB} = 8 \ \mu m\) and \(\Delta \gamma_{pl} = 0.002\).

The qualitative observations made in Figure 4 are echoed in Figure 5. Coatings with increasing thickness had stronger suppression effects on the operation of PSBs. This is reflected by the consistently lower shear strain magnitudes in PSBs that interacted with thicker coatings. Comparing Figure 5a–d, the suppression effects were attenuated significantly with the increasing applied strain amplitude. This is concomitant with the increasing plastic shear strain in the PSBs near the coating–substrate interfaces as the loading amplitude increases. For instance, at a lower applied strain range (such as at 0.002 for the case of \(d_{PSB} = 8 \ \mu m\) as shown in Figure 5d), the coatings had a profound effect suppressing the plastic shear strains near the coating–substrate interface. With a coating thickness of 0.5 \(\mu m\), the shear strain within the distance of 0.5 \(\mu m\) from the interface was lower than the prescribed 1% magnitude. With a coating thickness of 2 \(\mu m\), this distance extended beyond 2 \(\mu m\). However, at a higher applied plastic shear strain range of 0.01, this distance reduced to 0.13 \(\mu m\) for the thinner coating and \(\sim 1.3 \ \mu m\) for the thicker coating, shown in Figure 5a. The attenuation at higher strain amplitudes (smaller \(d_{PSB}\)) can be ascribed to the close coupling of neighboring PSB–substrate interactions, which induced larger elastic deflections within the coatings. As will be demonstrated in the later sections, this coupling also influences the stresses at/near the coating–substrate interfaces.

3.2. Fracture Tendency within the Coatings (Distribution of \(\sigma_{zz}\) in the Coatings)

Hard coatings, especially ceramic ones, may fracture from pre-existing flaws due to tensile stresses parallel to the coating layer. As shown in the third column of Figure 4a,b, the tensile stress (\(\sigma_{zz}\)) in the coating appear to rise at the locations where PSBs intersect with the coating for specimens at a small coating thickness of \(t_{coat} = 0.5 \ \mu m\). In addition, due to the load transfer from the substrates to the coatings, \(\sigma_{zz}\) is discontinuous across the interface. Due to the superposition of the neighboring PSB–coating interactions, the maximum \(\sigma_{zz}\) may be higher at a smaller PSB spacing (higher applied strain ranges). As an example, the profiles of \(\sigma_{zz}\) in the coating near the interface along the z-direction (i.e., values on the dashed lines shown in Figure 4) are plotted in Figure 6 for the 0.5-\(\mu m\) thick coating.

The observations made from Figure 4 are confirmed in the \(\sigma_{zz}\) profiles shown in Figure 6, noting the values of the stress within the blue shades (locations on the interfaces where PSBs intersect with the coatings). At higher applied strain amplitudes (such as the 0.01 plastic strain range reflected by \(d_{PSB} = 1 \ \mu m\), Figure 6a), both the overall and the peak values of the \(\sigma_{zz}\) are higher compared to lower applied strain amplitudes, indicating a higher tendency to develop tensile fracture, as expected. Figure 7a shows the variation of the peak \(\sigma_{zz}\) values as a function of \(d_{PSB}\) (reflecting the applied strain amplitude \(\Delta \gamma_{pl}\)), demonstrating a similar decreasing trend of the peak \(\sigma_{zz}\) with increasing \(d_{PSB}\) for all \(t_{coat}\) values.
when the thickness of the coating is large, the distribution of the 
Crystals in the coatings at the interface were nearly identical (see the thick and the thin dashed lines). However, 
z-direction at both the surface and the interface. In both coating thicknesses shown, the profiles of 
\( \sigma \) at the interface, of the computational cells with 0.5- 
values of the stress within the blue shades (locations on the interfaces where PSBs intersect with 
amplitude 
\( \Delta \gamma \) corresponds to \( \Delta \gamma_{pl} = 0.01 \), \( \Delta \gamma_{pl} = 0.004 \), and \( \Delta \gamma_{pl} = 0.002 \).

Figure 6. Stress profiles, including the \( \sigma_{zz} \) in the coating near the interface, \( \sigma_{xx} \) at the interface, and \( \tau_{xz} \) at the interface, of the computational cells with 0.5-\( \mu \)m coating thickness. The blue shades indicate the locations where the PSBs intersect with the coatings. Note that the horizontal axes are not of the same scale, which led to their different appearance in thickness. The four panels respectively show data for (a) \( d_{PSB} = 1 \mu \)m and \( \Delta \gamma_{pl} = 0.01 \), (b) \( d_{PSB} = 2 \mu \)m and \( \Delta \gamma_{pl} = 0.007 \), (c) \( d_{PSB} = 4 \mu \)m and \( \Delta \gamma_{pl} = 0.004 \), and (d) \( d_{PSB} = 8 \mu \)m and \( \Delta \gamma_{pl} = 0.002 \).

Figure 7. The maximum stresses, including (a) \( \sigma_{zz} \) in the coating at the interface, as well as (b) \( \sigma_{xx} \) and (c) \( \tau_{xz} \) at the interface, as functions of the increasing PSB spacing, \( d_{PSB} \). Note that the applied plastic shear strain range is inversely related to \( d_{PSB} \)—i.e., \( d_{PSB} = 1 \mu \)m corresponds to \( \Delta \gamma_{pl} = 0.01 \), \( d_{PSB} = 2 \mu \)m corresponds to \( \Delta \gamma_{pl} = 0.007 \), \( d_{PSB} = 4 \mu \)m corresponds to \( \Delta \gamma_{pl} = 0.004 \), and \( d_{PSB} = 8 \mu \)m corresponds to \( \Delta \gamma_{pl} = 0.002 \).

Comparing the third column of Figure 4c with that of the Figure 4a,b, it is interesting to note that when the thickness of the coating is large, the distribution of the \( \sigma_{zz} \) within the coating is less influenced by the presence of the PSBs. For instance, Figure 8 shows the profiles of \( \sigma_{zz} \) in the coating along the z-direction at both the surface and the interface. In both coating thicknesses shown, the profiles of \( \sigma_{zz} \) in the coatings at the interface were nearly identical (see the thick and the thin dashed lines). However,
for the case of a thin coating \((t_{\text{coat}} = 0.5 \, \mu m)\), significant variations in the stress can be observed on the surface (thin solid line). However, when the coating is thick \((t_{\text{coat}} = 2 \, \mu m)\), \(\sigma_{zz}\) is approximately invariant at the surface (thick solid line). The combined observations made in the third column of Figure 4 and in Figure 8 imply that a coating’s sensitivity to the presence of a potential surface flaw in the coating is different for different coating thicknesses. For instance, a thinner coating only experiences higher tensile stresses near the PSBs, a flaw at other locations may still be relatively safe and may not lead to early onset of fracture. On the other hand, the tensile stress on the surface of thicker coatings is uniform which makes thick coatings more susceptible to tensile fracture from surface flaws.

![Figure 8](image_url)

**Figure 8.** The profiles of \(\sigma_{zz}\) along the z-direction on both sides of the coating for two simulations: (1) \(t_{\text{coat}} = 0.5 \, \mu m, d_{\text{PSB}} = 1 \, \mu m\) and (2) \(t_{\text{coat}} = 2 \, \mu m, d_{\text{PSB}} = 1 \, \mu m\). The corresponding stress and strain contours of these two simulations have been shown in Figure 4a,c. The blue shade indicates the location where the PSBs intersect with the coating.

To further investigate the variation of \(\sigma_{zz}\) at different locations within the coating, its standard deviation (SD) along the z-direction for all model geometries was calculated. Figure 9 shows the SD of \(\sigma_{zz}\) at interface and the coating surface with respect to the ratio of \(d_{\text{PSB}}\) to the coating thickness \(t_{\text{coat}}\) (i.e., \(\lambda = d_{\text{PSB}}/t_{\text{coat}}\)). It is evident that, as the ratio \(\lambda\) increases (i.e., thickness of the coating decreases with respect to the PSB spacing), the variation of \(\sigma_{zz}\) along the z-direction at the coating surface significantly increases. On the other hand, the variation of \(\sigma_{zz}\) at the interface is always quite significant and is not affected by \(\lambda\). This agrees with the observations made earlier in Figure 8.

![Figure 9](image_url)

**Figure 9.** The standard deviation (SD) of \(\sigma_{zz}\) at two locations—i.e., at the coating–substrate interface and coating surface, versus the ratio \(\lambda = d_{\text{PSB}}/t_{\text{coat}}\).

3.3. Delamination Tendency at the Coating–Substrate Interface

The tendency for coating–substrate delamination was assessed by evaluating the interfacial stresses \(\sigma_{xx}\) and \(\tau_{xz}\), which were perpendicular and parallel to the interfaces, respectively. As shown in
Figure 4, due to the model setup of a perfectly bonded interface, both $\sigma_{xx}$ and $\tau_{xz}$ stress components were continuous across the interface. Similar to the behavior of $\sigma_{zz}$, $\sigma_{xx}$ appeared to slightly increase when the loading amplitude increased (i.e., when $d_{PSB}$ decreased). Interestingly, the magnitude of $\tau_{xz}$ showed an opposite trend—it appeared to decrease when the loading amplitude increased (i.e., when $d_{PSB}$ decreased). This can be seen by comparing Figure 4a, 4b in the second and the fourth columns. The opposite trends observed here may be ascribed to the “symmetries” in the $\sigma_{xx}$ and $\tau_{xz}$ values on both sides of the location where the PSBs intersect with the coating.

In Figure 6, the profiles of $\sigma_{xx}$ and $\tau_{xz}$ at the interface along the z-direction (i.e., values on the dashed lines shown in Figure 4) are plotted for the 0.5-µm coating thickness. At the PSB spacing of 8 µm, the interfacial stresses induced by an individual PSB is clear (see Figure 6d). The sign of the $\tau_{xz}$ component is opposite at the locations left and right of the intersection between the PSB and coating (see the red and blue arrows marking the $\pm \tau_{xz}$). On the other hand, the sign of the $\sigma_{xx}$ is the same on the left and right of this intersection—i.e., both values are positive (see the red arrows marking the $+\sigma_{xx}$ in Figure 6d). As a result, when the density of the PSB increases, the superposition of the stress fields from neighboring PSB–coating interactions increases the maximum magnitude of $\sigma_{xx}$ and reduces the maximum magnitude of the $\tau_{xz}$. The variation of the maximum $\sigma_{xx}$ and $\tau_{xz}$ stresses are discernable from Figure 6 by comparing the four panels. In addition, the magnitude of both stress components also increased with increasing coating thickness (compare Figure 4a and Figure 4c in the second and fourth columns). The $\sigma_{xx}$ and $\tau_{xz}$ appeared to somewhat signify the “suppressive” action of the coatings—as a function of the thickness—on the operations of the PSBs (compare Figures 4 and 5). In other words, the suppressive effects tend to be stronger when the values of these stresses increase.

For a clearer comparison, the peak values of these stresses for all the simulations have been obtained and plotted in Figure 7b,c. The substantial increases in the peak $\sigma_{xx}$ and $\tau_{xz}$ values due to the increase in the coating thickness are also evident. The combined action of the two stresses may be responsible for the delamination of the coating–substrate interface. This is in line with the critical plane approach put forth by Fatemi and Socie [47], which stated that the planes with large plastic shear strain and large normal stress tend to initiate fatigue cracks.

Figure 5 has shown that the suppression imposed by the coating on the operation of the PSBs is more effective at larger coating thicknesses. Nevertheless, excessively thick coatings are associated with the risk of early crack initiation due to coating tensile fracture (with pre-existing surface flaws) and coating–substrate delamination (due to the combined action of both tensile and shear stresses at the interface). Therefore, thicker coatings are only preferred if a coating with higher fracture toughness as well as an ideal coating–substrate adhesion can be achieved. Otherwise, thicker coatings may be detrimental to the fatigue performance of the coated parts.

On the other hand, while the applied plastic shear strain range is expected to monotonically affect the tendency of tensile fracture in the coating (i.e., higher amplitude leads to easier fracture), its effect on coating–substrate delamination may be more complex. Since the increase in the applied strain range decreases $\tau_{xz}$ but increases $\sigma_{xx}$, there may exist an intermediate plastic shear strain amplitude that favors delamination the most, assuming that the interfacial delamination is driven by the combined action of normal and shear stresses.

4. Conclusions

Crystal plasticity–based simulations were used to investigate the suppressive effects of coatings on the operation of surface PSBs. The impact of both coating thickness and the applied strain amplitude (reflected by a variable density of PSBs) on the suppressive effects were evaluated. Four characteristics of the PSB–coating interactions—including (1) the suppressive effects of coatings on the operation of PSBs, (2) the normal stress developed in the coating layer along the loading direction, (3) the interfacial normal stress developed perpendicular to the interface, and (4) the interfacial shear stress developed parallel to the interface—were investigated.

The following conclusions can be drawn from this research:
(1) Assuming a perfect coating–substrate adhesion and the absence of coating fracture, thicker coatings offered better suppression against the plastic shear deformation of the PSBs.

(2) The suppression effects of the coatings were attenuated at higher applied plastic shear strains (higher PSB densities).

(3) The distribution of the normal stress parallel to the loading direction in thinner coatings was highly heterogeneous and was strongly affected by the PSBs. However, the distribution of this stress was much more uniform for thicker coatings.

(4) The interfacial shear stress parallel to the loading direction and the interfacial normal stress perpendicular to the interface increased significantly with increasing coating thickness, which can potentially result in delamination.

(5) The peak values of the stresses mentioned in Conclusions (3) and (4) varied differently with increasing applied strains due to the superposition of the stress fields caused by the neighboring PSB–coating interactions.

In general, although thicker coatings may be beneficial to the fatigue performance of the coated parts, excessive coating thickness can lead to early crack initiation due to coating tensile fracture and coating–substrate delamination. The beneficial effect of the coatings on fatigue performance therefore is limited by the fracture toughness of the coating, and the adhesion strength of the coating–substrate interfaces. Therefore, the enhancement in the fatigue performance of a coating–substrate system hinges upon the careful selection of the correct coating–substrate material combination as well as the appropriate coating thickness.

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