Load compensation bridge for Josephson arbitrary waveform synthesizers

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Abstract
The Josephson arbitrary waveform synthesizer is a quantum-based voltage source that can generate arbitrary waveforms with quantum accuracy. However, these state-of-the-art performances are drastically decreased by the wiring connecting the source to the device under test. This wiring introduces deviations from the Josephson voltage which scale quadratically with frequency.

This paper describes a load compensation bridge that fully compensates the load of the Josephson arbitrary waveform synthesizer by the input impedance of the device under test and completely suppresses the frequency dependence up to a frequency of 80 kHz with an overall uncertainty of 2.8 \( \mu V V^{-1} \).

Keywords: impedance comparison, AC Josephson voltage standard, JAWS, digital bridge

(Some figures may appear in colour only in the online journal)
Since none of the previous attempts has lead to satisfactory results, a different approach needed to be developed that cancels the loading effect of the cable and decreases the difference between the voltage applied to the DUT and the calculated voltage at the Josephson junction array. This paper presents an original method based on a load compensation bridge (LCB) and shows its practical realisation as well as a set of convincing preliminary results.

2. Josephson arbitrary waveform synthesizer

For the proof of principle experiment, the LCB was combined with a JAWS system based on a pulse driven Josephson array with 12000 quad-stacked junctions [9]. The array was placed in a liquid helium Dewar using a cryoprobe. The Josephson junctions are driven by pulses provided by a ternary pulse-pattern generator (PPG) which was operated with a clock frequency of around 14 GHz.

The delta-sigma codes used for this LCB setup were of 2nd order, making the measured spurious free dynamic range (SFDR) of the JAWS system itself larger than 108 dB at 1 kHz. This value is comparable to the specification of the measurement device [10]. The quantum locking range (QLR) is the range where the various bias parameters can be changed without a change in the measured spectrum. These QLR were determined with the LCB (passive) and the Fluke 792A connected. The working point of each bias parameter was chosen to be close to the center of the QLR. These values were measured once at the beginning of the measurement period and stored to a settings file. All parameters were regularly checked (see an example in the results section), by determining the QLR of all the bias parameters again. No changes were observed during the measurement period. Figure 1 shows a spectrum measured at the input of the Fluke 792A at a frequency of at 1 kHz with the complete setup connected.

For this LCB setup the cryoprobe has a triaxial cable and connector for the voltage output. The compensation current for the ac-coupling [11] was delivered by a commercial function generator and a home made electronic source via a 50Ω coaxial line. One further line was used to connect the reference potential to the Josephson array (see figure 2).

Since the Josephson junctions are arranged within a coplanar waveguide, the array has an intrinsic inductance. This inductance causes a voltage drop of $i_{\text{out}} = 2\pi f L$. Where $f$ is the signal frequency, $I$ is the compensation current driven trough the array with the inductance $L$. The measured inductance of the array is about 15 nH. With the needed compensation current $I$ of about 2 mA, this causes an inductive voltage drop at 80 kHz, of about 15 μV over the array. This voltage is in quadrature with the 100 mV Josephson voltage and, therefore, adds quadratically to the voltage measured with the Fluke 792A. The maximum relative error introduced by this inductive voltage is around 1 part in 10⁸ and hence negligible for the present measurements.

3. Load compensation bridge

The setup of the load compensation bridge (LCB) is depicted in figure 2 and in the schematic of figure 3 to clarify the bridge’s principle. The Josephson voltage, $V_{\text{in}}$, is brought to the DUT by a triaxial cable. The current, $i$, flowing in the central conductor of this cable, is measured by a 1:100 detection transformer coupled to an ADC (voltage $V_i$). This current $i$ can be nulled by injecting a current $i_s$ through an impedance $Z_s$ which is biased by a DAC (voltage $V_s$), feeding a 1:1 double shielded injection transformer. In addition, at the injection point, the first shield of the triax-cable (coloured in blue in figure 2) is connected to the central conductor, forming an active guard, which prevents capacitive current from loading the system [12]. When $i = 0$, the voltage at the DUT, $V_{\text{out}}$, is expected to be equal to the input voltage $V_{\text{in}}$, i.e. the Josephson voltage.

At this point, a couple of important comments must be made:

- The distance between the reference planes (dotted lines in figure 2) for the voltages $V_{\text{out}}$, $V_{\text{in}}$ and the detection point—where $i$ is measured—has to be identical.
- The requirements on the stability and noise of the voltage $V_i$ is mitigated by a factor $Z_c/Z_{\text{in}}$, in which $Z_c$ is the impedance of the connecting cable of the JAWS. This factor can be made as small as $10^{-4}$ by choosing a high value for $Z_c$ (see [13] for a detailed description).
- When the bridge is balanced, no current flows through the central conductor of the cable. Therefore, a variation of its impedance, due to a variation of the He-level, will have a negligible effect on the voltage $V_{\text{out}}$ applied to the DUT.
The hardware components like the detection and injection transformers are home made. The DACs and ADCs are National Instrument multi-purpose boards type NI PXI 4461 which limit the maximum frequency to 80 kHz.

To connect the LCB to the Josephson junction array, the cryoprobe had to be custom wired with triaxial wiring. The length of this wire ($L_1$ in figure 2) had to be determined precisely to match the length of the LCB cables ($L_2$ in figure 2), according to the comment above. For this specific setup the length $L_1$ and $L_2$ were matched to within ±5 mm. The mechanical matching of the wiring will ensure that the electrical length (i.e. the length determining the impedance of the line) of both side of the wiring will be as close as possible.

The output voltage of the LCB is read by a freshly calibrated Fluke 792A thermal transfer standard coupled to a digital multimeter (Keysight 3458A).

The software controlling the LCB-running on the master computer—is able to balance the bridge fully automatically for a given set of frequencies and voltages making overnight measurement possible. The full automation requires that the LCB software also control the JAWS software-running on a slave computer—to select any required voltage and frequency. This was achieved using a LabVIEW TCP protocol. Finally, the LCB software also reads the output voltage of the Fluke 792A through the multimeter.

Both the JAWS system and the LCB bridge are synchronized on the same 10 MHz clock [14] to allow coherent sampling of $V_i$ and coherent generation of $V_S$. Moreover, the data processing and the balance procedure are fully described in [15].

### 4. Results

The measurements carried out were based on ac–ac differences performed at constant amplitude. The reference frequency was chosen to be 1 kHz, a frequency at which the effect of capacitive loading is known to be much smaller than 1 µV V$^{-1}$. After every high-frequency measurement, a control measurement at 1 kHz was performed to take the drift of the instruments into account. The relative difference $\Delta V/V_{1 \text{kHz}} = (V - V_{1 \text{kHz}})/V_{1 \text{kHz}}$ between the control measurement and the high-frequency result is reported in the graphics.

The effect of the LCB is demonstrated in figure 4. The quadratic frequency dependence observed when the LCB is not active is in agreement with previous measurements with similar systems [4, 6, 16]. Deviations as large as a few hundred of µV V$^{-1}$ are observed at 80 kHz. Once balanced the LCB has a dramatic effect on the measurements i.e. the quadratic
The background is severely suppressed. To gain further insight in the LCB performances the data at 100 mV are plotted alone in an enlarged scale in figure 5. At that scale the raw data (blue diamonds in figure 5) still reveal a non-negligible frequency dependence. The uncertainty bars on the data points are 1.7 \( \mu \text{V V}^{-1} \) (Type A uncertainty with \( k = 1 \)).

However, these data must be corrected with the calibration values of the Fluke 792A thermal transfer standard. The corrected data are plotted as red diamonds in figure 5. The final result is striking: the frequency dependence has been completely suppressed within the measurement uncertainties. The uncertainty bars are for a coverage factor of \( k = 1 \).

For the full determination of the uncertainty budget, two additional effects will have to be evaluated:

- The length of the cable injecting the current in the central conductor will produce a change in the phase of the current injected in the bridge.
- The influence of the length difference (\( \Delta L = L_1 - L_2 \)) between the triaxial cables connecting the JJA and the bridge will affect the equilibrium of the bridge.

1.4 \( \mu \text{V V}^{-1} \). This standard deviation is smaller than the uncertainty of the individual data points which is 2.8 \( \mu \text{V V}^{-1} \). For these corrected data, the type A uncertainty had to be combined with the calibration uncertainty of the Fluke 792A (in the 220 mV range) which is the dominant factor.

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- The influence of the length difference (\( \Delta L = L_1 - L_2 \)) between the triaxial cables connecting the JJA and the bridge will affect the equilibrium of the bridge.
Finally, the quantum locking range of the JAWS must be periodically checked during the course of the measurements to ensure that the pulse driven array (JJA) really works as a quantum standard. The output voltage of the JJA must be independent of any of its bias parameters over a certain range. An example of the measurement of the quantum locking range is shown in figures 6 and 7, where the output voltage is shown to be independent of the pulse amplitude (both positive and negative) and of the compensation current, thus providing confidence in the appropriate functioning of the JAWS.

5. Conclusion

This paper has shown that the original approach undertaken in this work by implementing a load compensation bridge is extremely successful. Using an active guard to compensate the capacitive current drawn by the system wiring, the quadratic frequency dependence present at the output terminal of the JAWS was completely eliminated within the measurement uncertainties. Presently, the uncertainty of the load compensation bridge is limited by the calibration of the DUT and amounts to 2.8 \( \mu \text{V V}^{-1} \) for a voltage of 100 mV and frequencies up to 80 kHz \( (k = 1) \). The influence of several additional parameters must be studied in details to expend its working range (both in frequency and voltage) and to further reduce its uncertainty. This paper must be considered as a first preliminary attempt that will certainly be completed by additional systematic studies in the near future.

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