Numerical Simulation 3D of Local Scour around Subsea Caisson Structures in Steady Currents and Waves

Xuyen Hoang*
College of Harbor, Coastal and Offshore Engineering
Hohai University, No.1 Xikang Road
Nanjing 210098, China
*Corresponding author

Abstract—This paper studied the local scour processes at subsea structures using using the computational fluid dynamics codes (OPENSOURCE CODE). The model solved the fully three-dimensional, Reynolds-averaged Navier–Stokes equation closed with the LES model. Stokes and Cnoidal Waves were generated using Fenton’s Fourier series method. Two empirical models must be used to compute the boundary layer at the interface and bed-load transport. We used the types of structured Cartesian grids. The velocity amplification at the corners is the dominant flow mechanism that controls the maximum scour depth. The results were agreement with the experimental study.

Keywords-local scour; horseshoe vortex; velocity amplification

I. INTRODUCTION

When a structure is placed in the flow pattern resulting in one or more of the phenomena: the flow accelerations at the corners, the horseshoe vortex at the upstream boundary and the vortex shedding behind the caisson. The investigations of obstruction have been presented by [1]; [2]. Several formulas for estimating local scour depth have been proposed by dimensional analyses by [2] or the analytical approaches [3]. More extensive studies which occur around a bridge pier have been classified: (1) scouring parameters concerning flow or sediment characteristics [4]; (2) effect of pier characteristics on scour depth [5]; (3) estimation of maximum scour depth [4] and most of the studies and (4) temporal variation of scour depth or geometry [6]. Two-dimensional numerical analyses by [7] or three-dimensional models with the hydrostatic assumption by [8] cannot reliably compute flow fields near the structure. Stokes and Cnoidal Waves were generated using Fenton’s Fourier series method. Because it is not possible to compute the flow dynamics about each individual grain of sediment and it is oftentimes difficult to compute the boundary layer at the interface, an empirical model must be used. This study is to answer the following questions: (1) What is the dominant flow mechanism that controls the maximum scour depth? Does the horseshoe vortex play a dominant role in the scour process?(2) How does the process of local scour occur around Caissons?

II. NUMERICAL MODEL

A. Flow Model

The governing equations for flow calculation are the Reynolds - Averaged Navier-Stokes equations

1) Momentum equations

The equations of motion for the fluid velocity components (u, v, w) in the three coordinate directions are the Navier-Stokes equations with some additional terms:

\[ \frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} = -\frac{1}{\rho} \frac{\partial p}{\partial x} + f_x + \frac{\partial (\rho u v)}{\partial x} \]

\[ \frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} = -\frac{1}{\rho} \frac{\partial p}{\partial y} + f_y + \frac{\partial (\rho u v)}{\partial y} \]

\[ \frac{\partial w}{\partial t} + u \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} + w \frac{\partial w}{\partial z} = -\frac{1}{\rho} \frac{\partial p}{\partial z} + f_z + \frac{\partial (\rho u w)}{\partial z} \]

2) Mass Continuity Equation

\[ \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0 \]

Where: \( p \) is the fluid density, \( R_{\text{SOR}} \) is a mass source. The velocity components (u, v, w) are in the coordinate directions (x, y, z). \( A_x \); \( A_y \) and \( A_z \) are area fractions for flow in the x, y and z directions.

B. Sediment Scour Model

The sediment scour model estimates the motion of sediment flow by predicting the erosion, advection and deposition of sediment.

\[ \frac{\partial c_{i,j}}{\partial t} + \nabla(u_c c_{i,j}) = 0 \]

Where \( c_{i,j} \) is the concentration of the suspended sediment, in units of mass per unit volume and \( u \) is the mean velocity of the fluid/sediment mixture. Therefore, one can write momentum balances for each sediment species and the fluid-sediment mixture.
Here: $u_{i,j}$ is the velocity of sediment species $i$; $\rho_{s,i}$ is the density of the sediment material; $f_{s,i}$ is the volume fraction of sediment species $i$; $P$ is the pressure; $K$ is the drag function.

The drift velocity is computed from the relative velocity using the definition of the drift and relative velocities:

$$u_{\text{drift}, j} = (1 - f_{s,j}) u^{\text{ref}, j} - \sum_{j=1}^{N-1} f_{s,j} u_{r,j}$$

C. Turbulence Transport Models

Large Eddy Simulation Model. The filter provides a formal definition of the averaging process and separates the resolvable scales from the sub grid scales. We use filtering to derive the resolvable-scale equation (Wilcox, D.C - 2006). For incompressible flow, the continuity and Navier-Stokes equations assume the following form.

$$\frac{\partial u_i}{\partial t} + \bar{u}_j \nabla u_{i,j} = -\frac{1}{\rho_s} \nabla P \frac{1}{\rho_s} \frac{\partial}{\partial x_j} \left( \nabla \cdot \bar{u}_i + f_{s,i} \delta_{ij} \right)$$

$$\rho \frac{\partial u_i}{\partial t} + \bar{u}_j \frac{\partial u_i}{\partial x_j} = \frac{1}{\rho_s} \nabla P + F - \frac{K}{f_{s,i} \rho_{s,i}} u_{r,i}$$

$$\frac{\partial \bar{u}_i}{\partial t} + \bar{u}_j \frac{\partial \bar{u}_i}{\partial x_j} = -\frac{1}{\rho_s} \nabla P + F$$

And scales velocity fluctuations by the magnitude of $L$ times the mean shear stress. These quantities are combined into the LES kinematic eddy viscosity

$$v_T = (cL)^2 \sqrt{2\epsilon_{ij} / 2\epsilon_{ij}}$$

where $c$ is the range of 0.1 to 0.2 and $\epsilon_{ij}$ denotes the strain rate tensor. This kinematic eddy viscosity is incorporated into the dynamic viscosity.

$$\mu = \rho (v + v_T)$$

D. Stokes and Cnoidal Waves Generator

Cnoidal Waves is a nonlinear oscillatory Wave in shallow water, which has sharper crests and flatter troughs than a Stokes Waves. It is generated using Fenton’s Fourier series method (Fenton-1999). Let $d$ and $H$ represent the undisturbed water depth and the Waves height (measured vertically from Waves trough to Waves crest), respectively. A stationary reference system $(x, z)$ is established in such a way that its origin is fixed at the bottom, $+x$ goes horizontally in the Waves propagation direction, and $+z$ directs vertically upward (when using the code, we can place the coordinate origin at any location but $+z$ must be in the upward direction). A current is assumed to exist and its $x$-component $u$ is a constant. The Waves speed $c$ and the angular Waves frequency $\omega$ are related to other parameters as

$$\omega = \frac{2\pi}{T} = ck$$

$$c = \frac{\lambda}{T}$$

where: $\lambda$ is the waves length; $k$ is the waves number and $T$ is the waves period.

The nonlinear equation system is iteratively solved using Newton’s method. Once the unknown variables are obtained, the transient water velocity in the stationary system $(x, z)$ is calculated using the following equations:

$$u(x, z, t) = \bar{u} + \sqrt{\sum_{j=1}^{N} jB_j \cosh jkz \cosh jkd} \cos jk(x - ct)$$

$$\omega(x, z, t) = \sqrt{\sum_{j=1}^{N} jB_j \sinh jkz \cosh jkd} \sin jk(x - ct)$$

Water elevation $\eta(x; t)$ is calculated using the Fourier transformation:

$$\eta(x, t) = \frac{E_0}{2} + \sum_{j=1}^{N+1} E_j \cos[(j - 1)(x - ct)]$$

where $E_j$ is calculated by numerical integration

$$E_j = \frac{2}{N} \sum_{n=1}^{N} \eta_n \cos[(j - 1)(n - 1)\pi / N]$$

for $j = 1, 2, ..., N + 1$
III. NUMERICAL SIMULATION AND VALIDATION

FIGURE 1 shows a computational domain for calculating scour around a subsea caisson. At the inlet boundary, the transverse and the vertical velocity components are set to zero. The computational domain (340×200×50) cm was divided into hexahedron 8-node tri-linear elements. The shapes of the caisson (X, Y): 40cm×20cm; Z=20cm; Steady currents V=35cm/s; Waves heights= 8cm. Water depth Hn=50cm; Waves period=2.5s; Mean fluid depth= 65cm;

| TABLE I. THE SCOUR RESULTS ARE SUMMARIZED |
|------------------------------------------|
| Cases | Simulation Results | Experimental Results |
|-------|--------------------|----------------------|
| Time  | 2s                 | 5s                   | 23.76 s               | 10 min | 1 h | 5 h |
| Scour depth (cm) | 3 | 6 | 12 | 4 | 8 | 15 |

Group 1: P11 Velocity (without Waves).
- Group 2: P22 Waves (without velocity).

Some parameters of experimental tests (B4) [9] are as follows: Water depth Hn=50cm; Velocity in X axis Vx=32.5cm/s; Specific gravity (s)=2.67; Diameter D50 mm=0.4; Critical shields parameter =0.066.

IV. 3D NUMERICAL SIMULATION RESULTS

The determination of stable scour depth: Stable scour depth is identified when mean kinetic energy is constant (See FIGURE. 2h).

- The flow accelerations at the corners. They appeared at 1/3 the horizontal length from the upstream corners (FIGURE. 2f). Fully non-hydrostatic pressure distributions closed and introduced the effect at sediment transport processes. (FIGURE. 2g)

- The horseshoe vortex at the upstream boundary (FIGURE. 2d) and vortex shedding behind (FIGURE. 2e). The horseshoe vortex plays a non-dominant role in the scour process. After 5 s of scour (See more FIGURE. 3b, 3e), the two scour holes at the upstream corners were deepened with the central part of the upstream and toward the two downstream corners. After 23.76 s of scour, the equilibrium scour depths at the two upstream corners were about 12 cm (FIGURE. 2c; 3c; 3f). The scour depth at the centre of the upstream boundary was 8 cm.
**V. CONCLUSIONS**

Local scour process around the subsea caisson was studied by 3D Numerical simulation. The mechanism of the scour was studied and the development of the stable scour depth and stable scour time was investigated. The results can be summarized as follows:

1. The velocity amplification at the corners of the caisson is the dominant flow mechanism that controls the maximum depth of scour around the structure. The waves, the horseshoe vortex plays a far less role than the velocity amplification.

2. The results of scour process indicated that although the input parameters of the simulations and the experiments are a little different but scour progress and the intensity scour are quite similar.

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