RELATIVISTIC POYNTING JETS FROM ACCRETION DISKS

R.V.E. Lovelace, and M.M. Romanova

Department of Astronomy, Cornell University, Ithaca, NY 14853-6801; RVL1@cornell.edu; Romanova@astro.cornell.edu

ABSTRACT

A model is derived for relativistic Poynting jets from the inner region of a disk around a rotating black hole which is initially threaded by a dipole-like magnetic field. The model is derived from the special relativistic equation for a force-free electromagnetic field. The “head” of the Poynting jet is found to propagate outward with a velocity which may be relativistic. The Lorentz factor of the head is

Γ = [B_0^2/(8πρ_0^2c^2)]^{1/6}

if this quantity is much larger than unity. For conditions pertinent to an active galactic nuclei, Γ ≈ (10/R)^(1/4)(B_0/10^4G)^(1/3)(1/cm^3/ρ_0)^(1/6), where B_0 is the magnetic field strength close to the black hole, ρ_0 = m_0 is the mass density of the ambient medium into which the jet propagates, R = r_o/r_g > 1, where r_g is the gravitational radius of the black hole, and r_o is the radius of the O-point of the initial dipole field. This model offers an explanation for the observed Lorentz factors ~ 10 of parsec-scale radio jets measured with very long baseline interferometry.

Subject headings: galaxies: nuclei — galaxies: magnetic fields — galaxies: jets — quasars: general

1. INTRODUCTION

Highly-collimated, oppositely directed jets are observed in active galaxies and quasars (see for example Bridle & Eilek 1984; Zensus, Taylor, & Wrobel 1998), and in old compact stars in binaries (Mirabel & Rodriguez 1994; Eikenberry et al. 1998). Further, well collimated emission line jets are seen in young stellar objects (Mundt 1985; Bührke, Mundt, & Ray 1988). Recent work favors models where the twisting of an ordered magnetic field threading an accretion disk acts to magnetically accelerate the jets (e.g., Merlí, Koida, & Uchida 2001; Bisnovatyi-Kogan & Lovelace 2001). There are two regimes: (1) the hydro-magnetic regime, where energy and angular momentum are carried by both the electromagnetic field and the kinetic flux of matter, which is relevant to the jets from young stellar objects; and (2) the Poynting flux regime, where energy and angular from the disk are carried predominantly by the electromagnetic field, which is relevant to extragalactic and microquasar jets, and possibly to gamma ray burst sources.

Different theoretical models have been proposed for magnetically dominated or Poynting outflows (Newman, Newman, & Lovelace 1992) and jets (Lynden-Bell 1996, 2003) from accretion disks threaded by a dipole-like magnetic field. Later, stationary Poynting flux dominated outflows were found in axisymmetric magnetohydrodynamic (MHD) simulations of the opening of magnetic loops threading a Keplerian disk (Romanova et al. 1998). MHD simulations by Ustyugova et al. (2000) found collimated Poynting flux jets. The present work represents a continuation of the studies by Li et al. (2001) and Lovelace et al. (2002; hereafter LO) which are closely related to the work by Lynden-Bell (1996). Self-consistent force-free field solutions are obtained where the twist of each field line is that due to the differential rotation of a Keplerian disk.

2. THEORY OF POYNTING OUTFLOWS

Here, we consider relativistic Poynting outflows from a rotating accretion disk around a Kerr black hole. We assume that at an initial time t = 0 an axisymmetric, dipole-like magnetic field threads the disk. The initial field geometry is shown in the lower part of Figure 1. This field could result from dynamo processes in the disk (e.g., Collinge, Li, & Pariev 1998). A more general magnetic field threading the disk would consist of multiple loops going from radii say r_a to r_b > r_a and r_c > r_b to r_d > r_c, etc. It is not clear how to treat this case analytically, but non-relativistic MHD simulations of this type of field show strong Poynting flux outflows (Romanova et al. 1998).

The disk is assumed to be highly conducting and dense in the sense that ρ_d(r)Ω^2 ≫ B^2/4π, ρ_d is the density and Ω(r) the angular rotation rate of the disk. Thus a magnetic field threading the disk is frozen into the disk. Further, we suppose that the radial accretion speed of the disk is much smaller than azimuthal velocity Ωr. For a corotating disk around a Kerr black hole

Ω = c^3/(GM) / (a_⋆ + (r/r_g)^{3/2})

for r > r_{ms} where r_{ms} is the innermost stable circular orbit, where a_⋆ is the spin parameter of the black hole with 0 ≥ a_⋆ < 1 and r_g ≡ GM/c^2. For example, for a_⋆ = 0.99, r_{ms} ≈ 1.45 r_g. The simplification is made that equation (1) also applies for r << r_{ms}. The region r ≤ r_{ms} has a negligible influence on our results for the considered conditions where the radial scale of the magnetic field r_o is such that (r_o/r_g)^{2} ≪ 1.

In the space above (and below) the disk we assume a “coronal” or “force-free” ideal plasma (Gold & Hoyle 1960). This plasma may be relativistic with flow speed v comparable to the speed of light. Away from the head of the jet, the electromagnetic field is quasi-stationary. This limit is applicable under conditions where the energy-density of the plasma γρc^2 is much less than the electromagnetic field energy-density (E^2 + B^2)/(8π).
Cylindrical \((r, \phi, z)\) coordinates are used and axisymmetry is assumed. Thus the magnetic field has the form \(\mathbf{B} = B_p \mathbf{\hat{r}} + B_\phi \mathbf{\hat{\phi}}\), with \(B_p = B_r \mathbf{\hat{r}} + B_z \mathbf{\hat{z}}\). We can write \(B_r = -(1/r)(\partial \Psi / \partial r)\), \(B_z = (1/r)(\partial \Psi / \partial r)\), where \(\Psi(r, z) \equiv r A_\phi(r, z)\) is the flux function. In the plane of the disk, the flux function is independent of time owing the frozen-in condition. A representative form of this function is

\[
\Psi(r, 0) = \frac{1}{2} \frac{r^2 B_0}{1 + 2(r/r_0)^2},
\]

where \(B_0\) is the axial magnetic field strength in the center of the disk, and \(r_0\) is the radius of the \(O\)-point of the magnetic field in the plane of the disk as indicated in Figure 1. Equation (2) is taken to apply for \(r \geq 0\) even though it is not valid near the horizon of the black hole. As already mentioned the contribution from region is negligible for the considered conditions where \((r_0/r)^2 \ll 1\). Note that \(\Psi(r, 0)\) has a maximum, with value \(r_0^2 B_0/6\), at the \(O\)-point where \(\mathbf{B}(r_0, 0) = 0\). For \((r/r_0)^2 \ll 1\), \(\Psi(r, 0) \propto r^2\) which corresponds to a uniform vertical field, whereas for \((r/r_0)^2 \gg 1\), \(\Psi(r, 0) \propto 1/r\) which corresponds to the dipole field \(B_2(r, 0) \propto -1/r^3\).

It is clear that equations (1) and (2) can be combined to give \(\Omega = \Omega(\Psi)\) which is a double valued function of \(\Psi\). The upper branch of the function is for the inner part of the disk \((r \leq r_0)\), while the lower part is for the outer part of the disk. A good approximation for the upper branch is obtained by taking \(\Psi \approx r^2 B_0/2\) which gives \(\Omega = (c^3 / GM) / [a_* + (2\Psi/B_0 r_0^2)]^{3/4}\).

The main equations for the plasma follow from the continuity equation \(\nabla \cdot (\rho \mathbf{v}) = 0\), Ampère’s law, \(\nabla \times \mathbf{B} = 4\pi \mathbf{J}/c\), Coulomb’s law \(\nabla \cdot \mathbf{E} = 4\pi \rho_c\), with \(\rho_c\) the charge density, Faraday’s law, \(\nabla \times \mathbf{E} = 0\), perfect conductivity, \(\mathbf{E} + \mathbf{v} \times \mathbf{B} = 0\), with \(\mathbf{v}\) the plasma flow velocity, and the “force-free” condition in the Euler equation, \(\rho_c \mathbf{E} + \mathbf{J} \times \mathbf{B}/c = 0\) (see for example Lovelace, Wang, & Sulkkanen 1987). Owing to the assumed axisymmetry, \(E_\phi = 0\), so that the poloidal velocity \(v_p = \kappa B_p\). Mass conservation then gives \(\mathbf{B} \cdot \nabla (\rho \kappa) = 0\), which implies that \(\rho \kappa = F(\Psi)/4\pi\), where \(F\) is an arbitrary function of \(\Psi\). In a similar way one finds that \(v_\phi - \kappa B_\phi = r G(\Psi)\), so that \(\mathbf{E} = -G(\Psi) \nabla \Psi\), and \(r B_\phi = H(\Psi)\), so that there are two additional functions, \(G\) and \(H\).

The function \(G\) is determined along all of the field lines which go through the disk. This follows from the perfect conductivity condition at the surface of the disk, \(z = 0\), \(E_z + (\mathbf{v} \times \mathbf{B})_z/c = 0\). This gives \(E_z = -(v_\phi B_z - v_z B_\phi)/c\), where \(v_\phi\) is zero at the disk and \(v_z\) is the disk velocity. Therefore, \(E_z(r, 0) = -\Omega (d\Psi(r, 0)/dr)/c\), so that \(G(\Psi) = \Omega(r)/c\) which gives \(\Omega = \Omega(\Psi)\).

The component of the Euler equation in the direction of \(\nabla \Psi\) gives the force-free Grad-Shafranov equation,

\[
\left[1 - \left(\frac{r \Omega}{c}\right)^2\right] \Delta^* \Psi = -\frac{\nabla \Psi}{2r^2} \cdot \nabla \left(\frac{r^4 \Omega^2}{c^2}\right) + HH' = 0 ,
\]

with \(\Delta^* \equiv \partial^2 / \partial r^2 - (1/r)(\partial / \partial r) + \partial^2 / \partial z^2\) and \(H' = \)
As mentioned above, we consider an initial value problem where the disk at $t = 0$ is threaded by a dipole-like poloidal magnetic field. The form of $H(\Psi)$ in equation (3) is then determined by the differential rotation of the disk: The azimuthal twist of a given field line going from an inner footpoint at $r_1$ to an outer footpoint at $r_2$ is fixed by the differential rotation of the disk.

Anmpère’s law gives $\oint d\mathbf{B} = (4\pi/e) \oint d\mathbf{J}$, so that $rB_\phi(r, z) = H(\Psi)$ is $(2/e)$ times the current flowing through a circular area of radius $r$ (with normal $z$) labeled by $\Psi(r, z) = $ const. Equivalently, $-H[\Psi(r, 0)]$ is $(2/e)$ times the current flowing into the area of the disk $r \leq r_m$. Our previous work (Li et al. 2000; L02) shows that $-H(\Psi)$ has a maximum so that the total current flowing into the disk for $r \leq r_m$ is $I_{tot} = (c/2)\langle H \rangle_{max}$, where $r_m$ is such that $-H[\Psi(r_m, 0)] = \langle H \rangle_{max}$ where $r_m$ is less than the radius of the O-point, $r_0$. The total current $I_{tot}$ flows out of the region of the disk $r = r_m$ to $r_0$.

For a given field line we have $d\phi/\mathbf{B}_p = ds_p/B_p$, where $ds_p = \sqrt{dr^2 + dz^2}$ is the poloidal arc length along the field line, and $B_p = \sqrt{B^2 + B_z^2}$. The total twist of a field line loop is

$$\Delta \phi(\Psi) = -\int_1^{r_2} ds_p \frac{B_p}{B_p} = -H(\Psi) \int_1^{r_2} ds_p r^2 B_p , \quad (4)$$

with the sign included to give $\Delta \phi > 0$. The integration goes from the disk at a radius $r_1 < r_0$ out into the corona and back to the disk at a radius $r_2 > r_0$. For a prograde disk the field line twist after a time $t$ is $\Delta \phi(\Psi) = \Omega(r_0) t [\Omega(r_1)/\Omega(r_0) - \Omega(r_2)/\Omega(r_0)]$.

2.1. Poynting Jets

Our previous study of non-relativistic Poynting jets by analytic theory (L02) and axisymmetric MHD simulations (Ustyugova et al. 2000) showed that as the twist, as measured by $\Omega(r_0) t$, increases a new, high twist field configuration appears with a different topology. A “plasmoid” consisting of toroidal flux detaches from the disk and propagates outward. The plasmoid is bounded by a poloidal field line which has an X-point above the O-point on the disk. The occurrence of the X-point requires that there be at least a small amount of dissipation in the evolution from the poloidal dipole field and the Poynting jet configuration. The high-twist configuration consists of a region near the axis which is magnetically collimated by the toroidal $B_z$ field and a region far from the axis which is anti-collimated in the sense that it is pushed away from the axis. The field lines returning to the disk at $r > r_0$ are anti-collimated by the pressure of the toroidal magnetic field. The poloidal field fills only a small part of the coronal space.

In the case of relativistic Poynting jets we hypothesize that the magnetic field configuration is similar that in the non-relativistic limit (L02, Ustyugova et al. 2000). Thus, most of the twist $\Delta \phi$ of a field line of the relativistic Poynting jet occurs along the jet from $z = 0$ to $Z(t)$ as sketched in Figure 1, where $Z(t)$ is the axial location of the “head” of the jet. Along most of the distance $z = 0 - Z$ the radius of the jet is a constant and $\Psi = \Psi(r)$ for $Z \gg r_0$.

Note that the function $\Psi(r)$ is different from $\Psi(r, 0)$ which is the flux function profile on the disk surface. Hence, $r^2 d\phi/dz = r B_\phi(r, z)/B_\phi(r, z)$, which is taken for simplicity that $\Psi = dz/dt = $ const. We determine $\Psi_z$ in §3. In this case, $H(\Psi) = 1^2 \Psi(\Psi)/V_c B_z$, where the right-hand side can be written as a function of $\Psi$ and $d\Psi/dr$. This relation allows the closure of equation (3) which can now be written as

$$\frac{d^2 \Psi}{dr^2} + \lambda \frac{1 - 1 \frac{d\Psi}{dr}}{\Psi} + \frac{\lambda + 1}{\lambda + 1} \left( \frac{d\Psi}{dr} \right)^2 \frac{d\Psi}{dr} = 0 , \quad (5)$$

where $\lambda \equiv (r \Omega/c)^2[(c/V_z)^2 - 1] = (r \Omega/c)^2/(\Gamma - 1)^2$, and $\Gamma \equiv 1/(1 - V_z^2/c^2)^{1/2}$.

Solution of equation (5) is facilitated by introducing dimensionless variables. We measure the radial distance in units of the distance $r_0$ to the O-point of the magnetic field threading the disk (equation 2). We measure the flux function $\Psi$ in units of $\Psi_0 = r_0^2 B_0/2$. The fields are measured in units of $B_0$ which is the magnetic field strength at the center of the disk. Thus, $B_z = (2\bar{r})^{-1} d\Psi/rdr$. The disk rotation rate $\Omega$ is measured in units of $c^3/(GM)$ (equation 1). In terms dimensionless variables $\bar{r}$, $\Psi$, and $\bar{\Omega}$, equation (5) is the same with overbars on these three variables. Note also that $\lambda = \bar{\Omega}^2 \bar{R}^2 \bar{\Omega}^2/(\Gamma - 1)^2$, where $\bar{R}^2 \equiv (r_0/r_0^2) \gg 1$.

We consider solutions of eqn. (5) using the approximation to eqn. (2) of $\Psi(r, 0) = \bar{\Psi}$ which gives $\bar{\Omega} = 1/(a_+ + \bar{R}^3/\bar{\Psi}^{3/4})$. These solutions are close to those obtained using the full dependence $\Omega(\Psi)$. We then have $\bar{\Omega} = 1/(a_+ + \bar{R}^3/\bar{\Psi}^{3/4})$. In this approximation there is a unique self-similar solution to eqn. (5) for $\bar{\Psi} \approx 1/\bar{R}$ where $\bar{\Omega} \approx \bar{R}^{-3/2}\bar{\Psi}^{-3/4}$. This solution is $\bar{\Psi} = \bar{\Psi}^{3/4} / \bar{R}^2(\Gamma - 1)^{1/2}$, with $\lambda = 2$. The dependence on $r$ is the same as found in the non-relativistic case by L02. The dependence holds for $\bar{r}_1 = 2(\Gamma - 1)^{1/2} / \bar{r} < \bar{r}_2 = 2(\Gamma - 1)^{1/2} \bar{R}^{1/2} / 3^{1/2}$. At the inner radius $\bar{r}_1$, $\bar{\Omega} = 1/\bar{R}^2$, which corresponds to the streamline which passes through the disk at a distance $r = r_g$. For $\bar{r} < \bar{r}_1$, we assume $\bar{\Psi} \propto \bar{r}^2$, which corresponds to $B_z = \text{const}$. At the outer radius $\bar{r}_2$, $\bar{\Psi} = \bar{\Psi}_{max} = 1/\bar{R}$ which corresponds to the streamline which goes through the disk near the O-point at $r = r_0$. Note that there is an appreciable range of radii if $\bar{R}^{1/2} \gg 1$. The non-zero field components of the Poynting jet are $E_r = -\sqrt{2(\Gamma - 1)^{1/2} B_z}$, $B_z = -\sqrt{2} B_z$, and $B_z = \bar{e}(r^{-3/2}) /[2\bar{R}(\Gamma - 1)^{1/2}]$, which hold for $r_1 < r < r_2$. This electromagnetic field satisfies the radial force balance equation, $dB^2/dr + (1/r^2)d(r^2(B_e^2 - E_e^2))/dr = 0$, as it should. At the outer radius of the jet at $r_2$, there is a boundary layer where the axial field changes from $B_z(r_2)$ to zero while (minus) the toroidal field increases by a corresponding amount so as to give radial force balance. This gives $-r_2 B_z(r_2) = -H_{max} = 2I_{max}/c = (2/\sqrt{3})\bar{\Psi}(r_2)/r_2$ which is close the relation found in the non-relativistic case (L02).

3. FORCE BALANCE AT THE HEAD OF THE JET

In the rest frame of the central object the axial momentum flux-density is $T_{zz}$, where $T_{jk}, (j,k = 0, 1, 2, 3)$ is the usual relativistic momentum flux-density tensor. In the reference frame comoving with the front of the Poynting jet, a Lorentz transformation gives $T_{zz}' = T_{zz} + 2(V_z/c)T_{0z} + (V_z/c)^2T_{00}$, where $T_{zz} = (E_r^2 + B_e^2)/c^3$.
\[ B_x^2 / 8 \pi = (4 \Gamma - 3) / 8 \pi, \] where the last equality uses our expressions for the fields. Further, \( T_{00} = E_x B_0 / 4 \pi = B_x^2 / 4 (\Gamma - 1)^{1/2} / 8 \pi, \) and \( T_{00} = (E_x^2 + B_x^2 + B_z^2) / 8 \pi = B_x^2 (4 \Gamma - 1) / 8 \pi. \) Combining these equations gives \( T_{zz}^* = B_x^2 / 8 \pi. \) Since \( T_{zz}^* \) varies with radius, we take its average between \( r_1 \) and \( r_2 \) which gives \( T_{zz}^* = B_x^2 / [8 \pi R^2 (\Gamma - 1)^2]. \) assuming \( r_1 \ll r_2. \)

In the reference frame comoving with the head of the jet, force balance implies that the ram pressure of the external ambient medium \( \rho_{\text{ext}} \Gamma^2 v_z^2 \) is equal to \( < T_{zz}^* >. \) This assumes \( V_z \) much larger than the sound speed in the external medium; however, details of the shock(s) at the jet front are not considered here. Thus we have \( (\Gamma - 1)^3 = B_x^2 / [8 \pi R^2 \rho_{\text{ext}} c^2]. \) For \( \Gamma \gg 1, \)

\[ \Gamma \approx \frac{10^{1/3}}{R} \left( \frac{B_0}{10^{13} \text{G}} \right)^{1/3} \left( \frac{1/\text{cm}^3}{n_{\text{ext}}} \right)^{1/6}, \] (6)

where \( n_{\text{ext}} = \rho_{\text{ext}} / \bar{m}, \) with \( \bar{m} \) the mean particle mass. A necessary condition for the validity of eqn. (6) is that the axial speed of the counter-propagating fast magnetosonic wave (in the lab frame) be larger than \( V_z \) so that the jet is effectively ‘subsonic.’ This condition can be expressed as \( \Gamma^2 < v_A^2 / 2, \) where \( v_A \equiv [B^2 / (4 \pi \rho)]^{1/2} \) is the Alfvén speed in the comoving frame of the jet. The above-mentioned force-free condition is \( (v_A')^2 > 1. \) The other important condition is that \( R^2 = (r_0 / r_0) \gg 1 \) so that the jet energy is extracted mainly from the disk (rather than from the rotating black hole).

The derived value of \( \Gamma \) is of the order of the Lorentz factors of the expansion of parsec-scale extragalactic radio jets observed with very-long-baseline-interferometry (see, e.g., Zensus et al. 1998). This interpretation assumes that the radiating electrons (and/or positrons) are accelerated to high Lorentz factors \( (\gamma \sim 10^3) \) at the jet front and move with a bulk Lorentz factor \( \Gamma \) relative to the observer. The luminosity of the \( z \pm \) Poynting jet is \( \dot{E}_j = c \int_0^\infty rdr E_{B_0} / 2 = c B_0^2 R r_0^2 / 3 \approx 2.2 \times 10^{45} (B_0/10^{13})^2 (R/10) (M/10^9 M_\odot)^2 \text{erg/s}, \) where \( M \) is the mass of the black hole.

The region of collimated field of the Poynting jet may be kink unstable. The instability will lead to a helical distortion of the jet with the helix having the same twist about the \( z \)-axis as the axisymmetric \( \mathbf{B} \) field. A relativistic perturbation analysis is required including the displacement current. The evolution of the jet evidently depends on \( \Gamma \) the speed of propagation of the lateral displacement and the velocity of propagation of the “head” of the jet \( V_z. \) Relativistic propagation of the jet’s head may act to limit the amplitude of helical kink distortion of the jet.

For long time-scales, the Poynting jet is of course time-dependent due to the angular momentum it extracts from the inner disk \( (r < r_0) \) which causes \( r_0 \) to decrease with time \( (L_02). \) This loss of angular momentum leads to a “global magnetic instability” and collapse of the inner disk (Lovelace et al. 1994, 1997; L02) and a corresponding outburst of energy in the jets from the two sides of the disk. Such outbursts may explain the flares of active galactic nuclei blazar sources (Romanova & Lovelace 1997; Levinson 1998) and the one-time outbursts of gamma ray burst sources (Katz 1997).

We thank an anonymous referee for criticism which improved this work and Hui Li and Stirling Colgate for valuable discussions. This work was supported in part by NASA grants NAG5-9047, NAG5-9735, by NSF grant AST-9986936, and by DOE cooperative agreement DE-FC03-02NA00057. MMR received partial support from NSF POWRE grant AST-9973366.

**REFERENCES**

Bisnovatyi-Kogan, G.S. & Lovelace, R.V.E. 2001, New Astron. Rev., 45, 663

Bridle, A.H., & Eilek, J.A. (eds) 1984, in Physics of Energy Transport in Extragalactic Radio Sources, (Greenbank: NRAO)

Bührke, T., Mundt, R., & Ray, T.P. 1988, A&A, 200, 99

Colgate, S.A., Li, H., & Pariev, V.I. 2001, Proc. of 20th Texas Symposium on Relativistic Astrophysics, Eds. J.C. Wheeler & H. Mar-

tel, p. 259

Elkenny, S., Matthews, K., Morgan, E.H., Remillard, R.A., & Nelson, R.W. 1998, ApJ, 494, L61

Gold, T., & Hoyle, F. 1960, MNRRAS, 120, 89

Katz J.I. 1997, ApJ, 490, 633

Levinson, A. 1998, ApJ, 507, 145

Li, H., Lovelace, R.V.E., Finn, J.M., & Colgate, S.A. 2001, ApJ, 561, 915

Lovelace, R. V. E., Li, H., Koldoba, A. V., Ustyugova, G. V., & Romanova, M. M. 2002, ApJ, 572, 445

Lovelace, R.V.E., Newman, W.I., & Romanova, M.M. 1997, ApJ, 484, 628

Lovelace, R.V.E., Romanova, M.M., & Newman, W.I. 1994, ApJ, 437, 136

Lovelace R.V.E., Wang J.C.L., & Sullanke M.E. 1987, ApJ, 315, 504

Lynden-Bell, D. 1996, MNRAS, 279, 389

Lynden-Bell, D. 2003, MNRAS, 341, 1360

Meier, D.L., Koide, S., & Uchida, Y. 2001, Science, 291, 84

Mirabel, I.F., & Rodriguez, L.F. 1994 Nature, 371, 46

Mundt, R. 1985, in Protostars and Planets II, D.C. Black and M.S. Mathews, eds. Univ of Arizona Press, Tucson, 414

Newman, W.I., Newman, A.L., & Lovelace, R.V.E. 1992, ApJ, 392, 622

Romanova, M.M., & Lovelace, R.V.E. 1997, ApJ, 475, 97

Romanova, M.M., Ustyugova, G.V., Koldoba, A.V., Chechetkin, V.M., & Lovelace, R.V.E. 1998, ApJ, 500, 703

Scharlemann, E.T., & Wagoner, R.V. 1973, ApJ, 182, 951

Scharlemann, E.T., & Wagoner, R.V. 1973, ApJ, 182, 951

Ustyugova, G.V., Lovelace, R.V.E., Romanova, M.M., Li, H., & Col-

gate, S.A. 2000, ApJ, 541, L21

Zensus, J.A., Taylor, G.B., & Wrobel, J.M. (eds.) 1998, Radio Emission from Galactic and Extragalactic Compact Sources, IAU Colloquium 164, (Astronomical Society of the Pacific: San Francisco)