Observation of blue-shifted ultralong-range \( \text{Cs}_2 \) Rydberg molecules

J. Tallant,\(^1\) S. T. Rittenhouse,\(^2\) D. Booth,\(^1\) H. R. Sadeghpour,\(^2\) and J. P. Shaffer\(^1\)

\(^1\)Homer L. Dodge Department of Physics and Astronomy, The University of Oklahoma, 440 W. Brooks St, Norman, OK 73019, USA
\(^2\)ITAMP, Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, Cambridge, Massachusetts 02138

(Dated: May 1, 2014)

We observe ultralong-range blue-shifted \( \text{Cs}_2 \) molecular states near \( n s_{1/2} \) Rydberg states in an optical dipole trap, where \( 31 \leq n \leq 34 \). The accidental near degeneracy of \((n-4)l\) and \( ns \) Rydberg states for \( l > 2 \) in Cs, due to the small fractional \( ns \) quantum defect, leads to non-adiabatic coupling among these states, producing potential wells above the \( ns \) thresholds. Two important consequences of admixing high angular momentum states with \( ns \) states are the formation of large permanent dipole moments, \( \sim 15 - 100 \) Debye, and accessibility of these states via two-photon association. The observed states are in excellent agreement with theory. Both projections of the total angular momentum on the internuclear axis are visible in the experiment.

The observation of ultralong-range Rydberg molecules has piqued interest in few-body Rydberg interactions that occur in ultracold atomic gases \([1,3]\). The interaction for an exotic class of these systems, trilobite molecules, arises to first order from the zero-range pseudopotential scattering of a Rydberg electron from a ground state perturber. Generally, bound molecular states form when the electron-atom scattering length is negative. Part of the fascination with such molecules originates from the prediction that these molecules can possess massive permanent electric dipole moments, \( \sim 1 \) kDebye, making them amenable to electric field manipulation \([4]\). Large dipole moments are expected when high electron angular momentum hydrogenic degenerate manifolds are involved in the electron-atom scattering. Ultracold Rydberg molecules formed by two-photon association into \( \text{Rb}(ns) \) states were expected only to have an induced dipole moment \([1]\). It was later demonstrated theoretically and experimentally \([5]\) that due to the near integer quantum defect of \( \text{Rb}(ns) \), \( \mu_s = 3.13 \), nearby and nearly degenerate \((n-3)\) manifolds mixed highly localized trilobite-like states into the zeroth order symmetric \( ns \) states, giving them an observable permanent dipole moment, \( \sim 1 \) Debye, in the body-fixed frame.

Here, we report the spectroscopic observation of ultralong-range trilobite-like Rydberg molecules formed in an ultracold gas of Cs with large permanent electric dipole moments. The spectroscopic signature of these molecules is in excellent agreement with theoretical predictions and serves as a milestone for creating trilobite molecules with giant dipole moments. The unique features of these ultralong-range Rydberg molecules are threefold. First, these states are unexpectedly blue-shifted with respect to the \( \text{Cs}(ns) \) thresholds. This feature results from the fact that the fractional part of the \( \text{Cs}(ns) \) quantum defect is small, \( \mu_s = 4.05 \), and \((n-4)l\), \( l > 2 \), “trilobite” manifolds become nearly degenerate, and mix strongly with the \( ns \) states \([5]\), inducing non-adiabatic avoided crossings of the \( ns \)-dominated Born-Oppenheimer (BO) potential energy curves. Second, the energetic proximity to the degenerate high-angular momentum hydrogenic states results in the molecular wavefunction having hydrogenic character at the 1% level. Therefore, large permanent electric dipole moments \( (15-100) \) Debye are predicted for these molecules. The rather large hydrogenic character of the wave function is promising for generating trilobite molecules with kD dipole moments. Third, the position of the Cs trilobite states depends sensitively on the location of the \( p \)-wave \( e^- \)-Cs scattering resonance \([6]\), and therefore the present spec-

FIG. 1: (Color Online) (a) The \( n = 31 \) BO potential energy curves for \( M_J = \pm 1 \) (solid curves) and \( M_J = 0 \) (dashed curves) \( \text{Cs}_2 \) Rydberg molecules in the vicinity of the \( ns \) Rydberg threshold. Also shown are the low lying vibrational wave functions in the experimentally accessible region. The zero of energy is set to the appropriate \( 31s_{1/2} \) atomic Rydberg energy. (b) The experimentally observed spectra are shown in arbitrary units compared to the BO potentials. The line sticks give the positions of the predicted energies and relative transition strengths of the predissociating vibrational states. The two \( M_J = \pm 1 \) vibrational levels have permanent dipole moments of 33.5 and 37.4 D, respectively.
tra also serve as an indirect probe of the accuracy of the 
$^3P_1$ resonance position \[7\]. Unlike atoms in magnetic 
traps, both parallel and perpendicular projections of the 
magnetic quantum number (i. e. $M_J = 0, \pm 1$) are visible 
in this experiment because it is carried out in an optical 
dipole trap. These molecules dissociate to their parent 
atomic constituents.

In Fig. \[1\] we present the main result of this work. 
The observed blue-shifted Cs Rydberg molecular spec-
trum accurately correlates with the vibrational lines of the 
calculations for states near the Cs(31s) threshold. Both 
$M_J = 0, \pm 1$ molecular symmetries are present. The 
blue-shifted potential wells arise from the strong non-
adiabatic BO coupling of the 31s state with the localized 
$2\ell$, $\ell > 2$, states. The binding energies are most eas-
ily defined with respect to the $ns$ threshold as each BO 
potential is largely s-character in the region where the 
spectroscopic resonances are observed. The molecular 
features are broadened with increasing energy from the 
31s threshold. This can be understood to be the result of 
progressively larger permanent dipole moments, as the 
higher energy states have more high $l$ character in their 
electronic wave functions.

Relatively large densities and ultracold temperatures 
are required to efficiently create the ultralong-range Cs 
molecules. The Cs molecules are photoassociated inside a 
crossed far-off-resonance trap (FORT) which is loaded 
from a Cs vapor cell MOT. The experimental setup has 
been described elsewhere \[8\]. The crossed FORT is pre-
pared from a 10 W 1064 nm Yb fiber laser. The first 
arm of the cross is formed by copropagating the FORT 
beam with one axis of the MOT trapping laser. The Yb 
laser beam is focused to a spot size $(1/e^2)$ of $86 \mu \text{m} \pm 1.1$ 
$\mu \text{m}$. The focal spot size was verified with a CCD camera 
and the results in Ref. \[8\]. The first Yb beam is recy-
cled and focused back into the chamber with the same 
spot size. The Yb beam intersects the first beam of the 
FORT at $22.5^\circ$ creating a crossed trapping region which is 
slightly cigar shaped with a 2:1 aspect ratio. At 17 
W of power, the FORT depth is $\sim 1.5 \text{mK}$. The highest 
trap frequency is $2\pi \cdot 2.23 \text{ kHz}$ and the lowest trap 
frequency is $2\pi \cdot 445 \text{ Hz}$. The crossed FORT is loaded as 
in \[8\] to a peak density of $\sim 2 \times 10^{13} \text{ cm}^{-3}$. The 
density was verified with absorption imaging and Rydberg 
atom detection rates. To account for the combined ac 
Stark shifts of the ground and Rydberg states, the posi-
tion of the Rydberg state was measured inside the MOT 
and compared to the position of the Rydberg state in the 
crossed FORT. The measured average ac Stark shift is 19 
MHz.

The molecular states are excited using a two-photon 
process. The first step of the excitation is an infrared 
(IR) photon which is tuned 182 MHz red of the Cs $6p_{3/2}$ 
hyperfine manifold. The second photon is generated by a 
ing ring dye laser tuned near 512 nm. The infrared beam 
is sent through an acousto-optic modulator (AOM) and 
single-mode polarization-preserving fiber. The output is 
collimated to a size of $1 \text{ mm}^2$ and intersects the crossed 
FORT at an angle of $79^\circ$ with respect to the long axis 
of the cross. During excitation, this beam has $5 \text{ mW}$ of 
power. The green beam is also sent through an AOM and a 
single-mode polarization-preserving fiber. The output 
is copropagated with the second FORT beam and is fo-
cused onto the crossed region with a spot size of $44 \mu \text{m}$. 
The power used for excitation is $70 \text{ mW}$. The two-photon 
linewidth of the excitation pulses was measured inside of 
the MOT to be $< 3 \text{ MHz}$. 

To locate the positions of the molecular states, the 
green laser is scanned on the blue side of the $ns_{1/2}$ Ryd-
berg states while the IR laser remains locked 182 MHz 
below the Cs $6s_{1/2}(F = 3) \rightarrow 6p_{3/2}(F = 2)$ transition. 
An absorption spectrum is acquired by monitor-
ning the number of ions produced as a function of green 
laser frequency. The excitation pulses begin 20 ms after 
the crossed FORT has been loaded to let the uncaptured 
MOT atoms fall away. Each excitation pulse is $10 \mu \text{s}$ long 
and is immediately followed by an electric field pulse to 
project any positive ions onto a microchannel plate de-
tector where they are counted. The excitation step re-
peats at $1.0 \text{ kHz}$ and lasts 500 ms, at which time the green 
laser frequency is incremented by $1 \text{ MHz}$ and the crossed 
FORT is reloaded. The electric field used to extract the 
ions, $67 \text{ V cm}^{-1}$, is far below the ionization threshold of 
any Rydberg states in the experiment \[9\]. The FORT 
beam is used to photoionize any Rydberg atoms as well 
as the Rydberg atom constituents of the ultralong-range 
molecules. Ion signals corresponding to the Cs$^+_2$ mol-
ecular time-of-flight are simultaneously acquired with the 
Cs$^+$ signal. As many as six absorption spectra are aver-
gaged together with scaled frequencies to obtain a single 
experimental spectrum. Ions arriving at the molecular 
time-of-flight were not observed, suggesting a different 
decay mechanism than found in Ref. \[1\]. However, if the 
molecules gain $> 1 \text{ GHz}$ of energy, they will be lost from the 
ionization region.

Precise knowledge of the absolute frequencies of both 
excitation lasers is required to correctly describe the en-
ergies of observed molecular transitions. The absolute 
frequency of the IR beam is monitored with a saturated 
absorption setup. The light for the saturated absorp-
tion is shifted with AOMs such that the Cs $6s_{1/2}(F = 
3) \rightarrow 6p_{3/2}(F = 3)$ transition is on resonance during the 
experiment. The saturated absorption spectrum deter-
mines the IR frequency within $\sim 3 \text{ MHz}$. To monitor the 
frequency of the green laser, a fraction of the laser out-
put is combined with light from the IR laser to generate 
an electromagnetically induced transparency (EIT) sig-
nal in a room-temperature Cs vapor cell. The EIT setup 
is arranged in both co- and counterpropagating config-
urations with respect to the IR beam. This arrangement 
produces up to six EIT resonances corresponding to dif-
ferent hyperfine states and detunings whose absolute fre-
frequency relations are known. The positions of the EIT resonances can be shifted to any desired location with AOMs to provide spectroscopic markers.

The bonding of these types of Rydberg molecules derives from the frequent scattering of the highly excited Rydberg electron from the ground state atom perturber [5][6]. The relevant electron-ground state atom interaction is described within the zero-range Fermi pseudopotential approximation [11][12], given in atomic units by

\[ V_{e-a}(r) = 2\pi A_s(k) \delta^{(3)}(r - R) + 6\pi A_p^3(k) \delta^{(3)}(r - R) \frac{\nabla \cdot \nabla}{r^2} \]  \hspace{1cm} (1)

where \( A_s \) and \( A_p \) are the energy dependent s- and p-wave scattering length and \( r \) and \( R \) denote the positions of the electron and ground state atom relative to the Rydberg core, respectively. The BO potentials which support the molecular predissociating states are found by diagonalizing the interaction of Eq. (1) in a basis of Rydberg electron nl orbitals [5][6]. Within the semiclassical picture the electron wavenumber \( k \) is related to the intermolecular distance \( R \) in atomic units by \( k = \sqrt{2(1/R - E_b)} \) where \( E_b \) is the binding energy of the isolated Rydberg atom. The energy dependent scattering lengths are given by \( A_s(k) = -\tan \delta_s/k \) and \( A_p^3(k) = -\tan \delta_p/k^3 \) where \( \delta_s \) is the scattering phase shift for l-wave electron Cs scattering. Cs has relatively large spin-orbit interaction resulting in different (\( J = 0,1 \) and 2) e--Cs \( 3P_J \) resonant scattering phase shifts. To account for this, we take the p-wave scattering to be,

\[ A_p^3 = \sum_{J=0}^{2} \left[ C^{J|M_J|0,1M_J} \right]^2 A_{p,J}^3 \]  \hspace{1cm} (2)

where \( C^{J|M_J|0,1M_J} \) is a Clebsch-Gordan coefficient coupling the bound e- angular momenta (\( L_1 M_1 \)) to the scattering e- angular momenta (\( L_2 M_2 \)) to form the total angular momenta (\( J M \)). The different Clebsch-Gordan coefficients create different potentials for the \( M_J = \pm 1 \) and 0 cases. The p-wave scattering potentials are found by setting the \( 3P_1 \) resonance position to 8 meV [7] and the splitting of the \( 3P_0 \) and \( 3P_2 \) states to those of Ref. [13].

The resulting BO potentials near the ns Rydberg thresholds are shown for \( n = 31 - 34 \) in Figs. [1] and [2](b-d) respectively for total angular momentum projection \( M_J = \pm 1 \) (solid curves) and 0 (dashed curves). Fig. [2](a) shows the \( n = 31 \) BO potentials over a larger energy range correlating to atomic Rydberg thresholds in the vicinity of Cs(31s) state. The near degeneracy of the \((n-4)l > 2\) manifolds with the ns series ensures that there are non-adiabatic couplings between the molecular potential energy curves of the same symmetry. Two important consequences of this interaction are the formation of potential wells capable of supporting bound states, blue-shifted with respect to the ns Rydberg thresholds, and accessibility of these states via two-photon association. The latter is facilitated by the fact that the electronic wave functions for the molecular states contain large s-wave components. Figs. [2](b-d) also show several of the low lying vibrational wavefunctions within the experimentally accessible region. The averaged experimental data near the ns1/2 Rydberg states for \( n = 31 - 34 \) are compared with the theoretical predictions and show excellent agreement. All of the molecular states have spatial angular momentum projection \( M_J = 0 \) [14][15], i.e. all of the states are \( 3\Sigma \) molecules. While there exist BO potential energy curves corresponding to the \( 3\Pi \) symmetry, they do not couple to the molecular states considered here [4]. Because the BO potentials near the ns thresholds are sensitive to the position of the \( 3P_1 \) resonance, the agreement between theory and experiment can be used as an indirect probe of the accuracy of the resonance position [17]. Most of the observed states correspond to the \( M_J = \pm 1 \) projections of the electronic angular momentum, but because these states are photodissociated in a FORT, we are sensitive to the \( M_J = 0 \) projection as well. In all the spectra, we observe features corresponding to \( M_J = 0 \) states.

The molecules also experience an ac Stark shift in the FORT. As the molecular states consist of single Rydberg excitations, and the ac Stark shift of a Rydberg atom is only weakly dependent on the Rydberg state [9][14], we then expect that the Rydberg molecular states have the same overall shift and inhomogeneous broadening seen in the bare atomic transition. This hypothesis is corroborated by the fact that the observed data shifted by the measured atomic ac Stark shift, 19 MHz, are in good agreement with theory. However, the experimental widths of the most prominent states seen in Figs. [2](e-g) are \( \sim 20 \) MHz, far larger than that expected from the atomic Rydberg linewidth, \( \sim 100 \) kHz [15] and that observed for the Cs Rydberg atoms, \( \sim 11 \) MHz. The additional broadening is likely due to the existence of large dipole moments for the Rydberg molecules, \( \sim 30 \) D. We expect small stray electric fields (on the order of 100 mV cm\(^{-1}\)) coupled to the large molecular dipoles to produce broadening in the range of \( 4 - 10 \) MHz. The strength of the dipole moments increases with increasing energy above the Cs(ns) thresholds, as the molecular states progressively retain less and less s-wave character. The observed molecular spectra in Fig. [2](b) and [2](e-g) become progressively broadened with energy, lending further support to our assertion.

A molecule with a dipole moment of \( \sim 35 \) D should exhibit a dramatic linear Stark effect. A modest applied field of 240 mV cm\(^{-1}\) can produce a measurable shift. To investigate this, small background electric fields were applied during excitation of the two \( M_J = \pm 1 \) molecular states near \( n = 31 \). Surprisingly, even electric fields below 100 mV cm\(^{-1}\) cause changes in the observed spectrum. A linear Stark effect is not observed. Rather, the observed peaks broaden and slightly shift to
FIG. 2: (Color Online) (a) The BO potential energy curves for $M_J = \pm 1$ (solid curves) and $M_J = 0$ (dashed curves) correlating to atomic Rydberg thresholds in the vicinity of Cs(31 $s$) state. The $n = 32 - 34$ BO potential energy curves for $M_J = \pm 1$ (solid curves) and $M_J = 0$ (dashed curves) are displayed in (b-d) and the corresponding observed spectra are shown in (e-g), respectively. For detailed description of the features, see caption for Fig. 1. The zero on the energy axis refers to the corresponding Cs($ns$) threshold.

the blue ($\sim 10$ MHz) before the bluest peak disappears completely. The additional broadening of the lines decrease their amplitude and complicate the measurement. The effect is different for each of the observed molecular states, which is to be expected based on their different potential minima. Our observations cannot be simply described as a linear Stark shift because the potentials supporting the bound states are changing appreciably with the applied field. This is expected to be different than the Rb case [5] because the molecular states here have significant mixing with the degenerate hydrogenic manifold and are the result of avoided crossings, which are sensitive to the applied electric field. As a consequence, the electric field dependence of the Cs ultralong-range molecules studied is sufficiently complicated to prevent a full analysis in this paper.

In summary, we have observed Cs Rydberg molecular states in a crossed optical dipole trap and found the spectrum to be in excellent agreement with theory. The agreement with theory provides an experimental probe for the position of the p-wave resonance [7]. We observed both $M_J = 0$ and $M_J = \pm 1$ states, not easily observed in a magnetic trap. The molecular states studied have different properties than those reported earlier for Rb. There is significantly large mixing of the highly localized “trilobite-like” electronic character in Cs. The additional line broadening observed is believed to arise from the interaction of the large permanent electric dipole moment. We measured large changes in the spectrum by applying small electric fields, suggestive of both large permanent electric dipole moments and structural changes to the states, consistent with theory. In contrast with Rb, a large signal for the Cs$^2+$ molecular ion is not observed, suggesting a different decay mechanism. We will attempt to address the behavior of the molecular states in electric fields and understand their decay mechanisms. The discovery of spectroscopically accessible Cs trilobite states opens another window into these exotic molecules. It may be possible to use these states to create ion pair states. Applications that exploit their large permanent
dipole moments are sure to follow.

Acknowledgements

The authors thank C. H. Greene, T. Pfau, and L. Marcassa for helpful discussions. HRS and STR acknowledge support through an NSF grant to ITAMP at Harvard University and the Smithsonian Astrophysical Observatory. The experiment was supported by the NSF (PHY-0855324).

* Electronic address: [hsadeghpour@cfa.harvard.edu]
† Electronic address: [shaffer@nhm.ou.edu]
[1] V. Bendowsky, B. Butscher, J. Nipper, J. P. Shaffer, R. Löw, and T. Pfau, Nature, 458, 1005 (2009).
[2] K. R. Overstreet, A. Schwettmann, J. Tallant, D. Booth, and J. P. Shaffer, Nat. Phys., 5, 581 (2009).
[3] V. Bendkowsky, B. Butscher, J. Nipper, J. B. Balewski, J. P. Shaffer, R. Löw, T. Pfau, W. Li, J. Stanojevic, T. Pohl, and J. M. Rost, Phys. Rev. Lett., 105, 163201 (2010).
[4] C. H. Greene, A. S. Dickinson, and H. R. Sadeghpour, Phys. Rev. Lett., 85, 2458 (2000).
[5] W. Li, T. Pohl, J. M. Rost, S. T. Rittenhouse, H. R. Sadeghpour, J. Nipper, B. Butscher, J. B. Balewski, V. Bendkowsky, R. Löw, and T. Pfau, Science, 334, 1110 (2011).
[6] A. A. Khuskivadze, M. I. Chibisov, and I. I. Fabrikant, Phys. Rev. A, 66, 042709 (2002).
[7] M. Scheer, J. Thogersen, R. C. Bilodeau, C. A. Brodie, H. K. Haugen, H. H. Andersen, P. Kristensen, and T. Andersen, Phys. Rev. Lett., 80, 684 (1998).
[8] J. Tallant, D. Booth, and J. P. Shaffer, Phys. Rev. A., 82, 063406 (2010).
[9] T. F. Gallagher, Rydberg Atoms, 1st ed. (Cambridge University Press, 1994).
[10] C. Bahrim, U. Thumm, and I. I. Fabrikant, J. Phys. B, 34, L195 (2001).
[11] E. Fermi, Nuovo Cim., 11, 157 (1936).
[12] A. Omont, J. Phys. (Paris), 38, 1343 (1977).
[13] U. Thumm and D. W. Norcross, Phys. Rev. Lett., 67, 3495 (1991).
[14] K. C. Younge, B. Knuffman, S. E. Anderson, and G. Raithel, Phys. Rev. Lett., 104, 173001 (2010).
[15] B. Butscher, J. Nipper, J. B. Balewski, L. Kukota, V. Bendowsky, R. Löw, and T. Pfau, Nat. Phys., 6, 970 (2010).