Normalizing Weak Boson Pair Production at the Large Hadron Collider

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The production of two weak bosons at the Large Hadron Collider will be one of the most important sources of SM backgrounds for final states with multiple leptons. In this paper we consider several quantities that can help normalize the production of weak boson pairs. Ratios of inclusive cross-sections for production of two weak bosons and Drell-Yan are investigated and the corresponding theoretical errors are evaluated. The possibility of predicting the jet veto survival probability of $VV$ production from Drell-Yan data is also considered. Overall, the theoretical errors on all quantities remain less than $5 \div 20 \%$. The dependence of these quantities on the center of mass energy of the proton-proton collision is also studied.

I. INTRODUCTION

The physics potential of the Large Hadron Collider (LHC) is breath taking. The CMS and ATLAS experiments at the LHC are expected to shed light on the origin of mass and dark matter of the universe, and other crucial aspects involving physics beyond the Standard Model (SM) [1–3]. The investigation of the phase-space provided by the large center of mass energy of the proton-proton collision and the multiplicity of experimental signatures make the prospects of searches for the Higgs boson and physics beyond the SM at the LHC very exciting.

The search for new physics in final states with multiple charged leptons and missing transverse energy ($E_T^{miss}$) carried by neutrinos or other particles escaping detection is arguably one of the most interesting among the feasible signatures at hadron colliders. The presence of several isolated leptons reduces the contribution of expected SM processes, allowing for the exploration of physics beyond the SM in low $E_T^{miss}$ regions.

The search for $WW, ZZ$ resonances is central for the observation of the Higgs boson in a wide range of mass [4–14]. Several are the motivations for searches for physics beyond the SM with these final states. The production of multi-leptons is predicted by R-parity conserving [15–18] and violating [19] supersymmetry and nonminimal supersymmetric models [20]. The existence of massive neutrinos is a strong motivation for physics beyond the SM and in order to test their Majorana nature one has to investigate the possibility of observing them in different multi-lepton channels [21–26]. The phenomenology of the Littlest Higgs boson models with T-parity also predicts significant rates of multi-leptons [27]. Furthermore, kinematic properties of the production of multi-leptons can be used to disentangle models beyond the SM [28].

The production of two weak bosons ($VV$) at the LHC will be one of the most important sources of SM backgrounds for multi-lepton final states. The prediction of the rates of $VV$ will be instrumental in these searches. In this paper we consider several quantities that can help normalize the production of $VV$, as suggested in [29]. These quantities will have reduced uncertainties since the error due to the integrated luminosity measurement will cancel out, and the scale and parton density uncertainties will be diminished. Ratios involving the production of $VV$ and Drell-Yan are investigated and the corresponding theoretical errors are evaluated. In Section II we investigate a number of ratios to predict the inclusive rates of $ZZ, WW$ and $ZW$ production. In Section III we consider the possibility of predicting the jet veto survival probability of $VV$ with Drell-Yan. The latter is crucial to distinguish the multi-lepton backgrounds coming from $VV$ from those coming from the decays of top quarks.

The LHC is scheduled to deliver proton-proton collisions in 2009 and 2010 with a center of mass energy, $\sqrt{s} = 10$ TeV, after which efforts will be made to reach $\sqrt{s} = 14$ TeV [30]. The nominal results presented in this paper have been obtained for $\sqrt{s} = 14$ TeV, but we have also considered their dependence on lower values of $\sqrt{s}$.

\(^1\) In this paper by leptons we imply electron and muons only.
The inclusive rate of multi-leptons coming from the decay of VV can be predicted by multiplying the observed rate of di-leptons coming from the Drell-Yan process by the corresponding cross-section ratios $\frac{\sigma_{VV}}{\sigma_{Z^*}}$ (and $\frac{\sigma_{VV}}{\sigma_{W^*W^*}}$, when appropriate) computed theoretically. The uncertainty associated with these estimates arises from experimental and theoretical errors. The experimental errors arise primarily from the uncertainty of the rate of di-leptons coming from Drell-Yan and the error on the efficiency of observing multi-leptons coming from the decay of VV. The dominant theoretical errors are expected to arise from the uncertainty of the ratios $\frac{\sigma_{VV}}{\sigma_{Z^*}}$ due to QCD scale variations and uncertainties in the parton densities in the proton.

The results on $\frac{\sigma_{VV}}{\sigma_{Z^*}}$ (and $\frac{\sigma_{VV}}{\sigma_{W^*W^*}}$) shown in this Section are based on fixed order Matrix Element (ME) computations, including the decay products of the weak bosons. Cross-sections are computed for decays involving leptons of different flavor after the application of generic kinematic cuts. The renormalization and factorization scales are set to the average mass of the weak boson. The scale-related uncertainty is obtained by varying the renormalization and factorization scales by a factor of four. Here we change both scales at the same time in equal and in opposite directions and we take the maximum deviation for the quantity considered. We believe this choice of scales yields a conservative estimate of the scale-related error. The CTEQ6M [31] parton density parameterization is used, which also allows an estimate of the corresponding parton density uncertainties. We stress that results are obtained at parton level and no detector simulation is implemented. Our choice of electro-weak parameters corresponds to setting the Fermi constant, $G_F$ and the masses of the weak bosons and the top quark, $m_W$, $m_Z$, $m_t$, and then determining $\alpha_Z$ and $\sin^2\theta_W$ from them \(^2\).

### II. INCLUSIVE RATES

#### A. ZZ Production

Accurate predictions for the hadronic production of Z-boson pairs, including higher order QCD corrections, have been studied extensively in the literature [32–34]. The production of Z boson pairs through gluon-gluon fusion contributes at $\mathcal{O}(\alpha_s^2)$ relative to $q\bar{q}$ annihilation, but its importance is enhanced by the large gluon flux at the LHC. This process was first analyzed in Refs. [35, 36], with leptonic decays subsequently studied for on-shell [37] and off-shell [38] weak bosons. The first complete calculation of the gluon-induced loop process $gg \rightarrow Z^*(\gamma^*)Z^*(\gamma^*) \rightarrow \ell\ell\ell\ell$ \(^3\), allowing for arbitrary invariant masses of the Z bosons and including also the photon contributions, was presented in Ref. [39]. For Higgs boson searches with masses below the $Z^*$-pair threshold, the virtual photon contribution to the $Z^*(\gamma^*)Z^*(\gamma^*)$ background cannot be neglected, since one of the produced Z bosons will almost always be off-resonance. Here we focus on the production of two lepton pairs with invariant masses close to the Z mass.

A first attempt to relate the production of four leptons arising from ZZ production to di-lepton production from the Drell-Yan process in a proton-proton collision was reported in Ref. [40]. Although the next-to-leading order (NLO) QCD corrections to the $q\bar{q}$ initiated processes were taken into account, the necessary tools for the evaluation of the

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\(^2\) See http://mcfm.fnal.gov/ for more details.

\(^3\) For simplicity we sometimes refer to this process as $gg \rightarrow ZZ$. 

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### TABLE I: Cross-sections (in fb) for the $ZZ$ and $Z^*$ production at the LHC for different ranges of the invariant mass of the leptonic system, $m_{\ell\ell}$ (in GeV). The renormalization and factorization scales are set to be equal to the $Z$ mass. The event selection specified in Section II A is applied. Results are given for $\sqrt{s} = 14$ TeV.

| $m_{\ell\ell}$ range (fb) | \(\frac{\sigma_{Z^*\to \ell\ell}}{\sigma_{Z}}\) | \(\frac{\sigma_{Z^*\to \ell\ell}}{\sigma_{Z}}\) | \(\frac{\sigma_{Z^*\to \ell\ell}}{\sigma_{Z}}\) | \(\frac{\sigma_{Z^*\to FF}}{\sigma_{Z}}\cdot 10^3\) |
|--------------------------|-----------------|-----------------|-----------------|-----------------|
| 200 - 250                | 886.8           | 4.00            | 0.591           | 5.17            |
| 250 - 300                | 376.6           | 1.82            | 0.265           | 5.54            |
| 300 - 350                | 186.2           | 0.93            | 0.123           | 5.66            |
| 350 - 400                | 102.8           | 0.53            | 0.066           | 5.83            |
| 400 - 450                | 60.5            | 0.32            | 0.041           | 5.94            |
| 450 - 500                | 38.0            | 0.20            | 0.027           | 6.01            |
| 500 - 750                | 71.9            | 0.37            | 0.057           | 5.92            |
| 750 - 1000              | 13.7            | 0.08            | 0.016           | 6.88            |
contribution from the $gg \rightarrow ZZ$ diagrams referred to above were not available. These corrections are added in this paper.

We use the package MCFM for the computation of the cross-sections due to $q\bar{q} \rightarrow Z^*(\gamma^*)Z^*(\gamma^*) \rightarrow \ell\ell\ell\bar{\ell}$ in NLO QCD, $\sigma_{NLO}^{ZZ}$ [34]. The matrix elements for $gg \rightarrow Z^*(\gamma^*)Z^*(\gamma^*) \rightarrow \ell\ell\ell\bar{\ell}$ are implemented in the package $gg2ZZ$, a parton-level integrator and event generator [39] that we use to compute the corresponding leading order cross section, $\sigma_{LO}^{gg\rightarrow ZZ}$. The MCFM package is also used for the computation of the Drell-Yan QCD NLO cross-section $\sigma_{NLO}^{ZZ}$. Since a complete NNLO QCD description of $ZZ$ production is not available, a best estimate is obtained by summing the cross-sections $\sigma_{NLO}^{ZZ}$ and $\sigma_{LO}^{gg\rightarrow ZZ}$, treating them as independent processes.

We compute the cross-sections for $ZZ$ production with generic cuts on the decay products. It is required that each of the four leptons has a transverse momentum, $p_T > 20$ GeV and lies in the pseudorapidity range, $|\eta|<2.5$. For the comparison with the Drell-Yan cross-sections, it is required that the invariant mass of the lepton pairs be in the range $71 < m_\ell < 111$ GeV. The cross-sections for the Drell-Yan process are calculated by requiring two leptons with $p_T > 20$ GeV in the range $|\eta|<2.5$. It is required that the distance $\Delta R = \sqrt{(\Delta \phi)^2 + (\Delta \eta)^2}$ between leptons be greater than 0.2 and between the leptons and a parton be greater than 0.7. In both calculations the impact of internal photon bremsstrahlung is not taken into account, as it is expected to be small in the inclusive quantities we study here.

Table I displays the cross-sections for the $ZZ$ and $Z^*$ at the LHC for different ranges of the invariant mass of the leptonic system, $m_{N\ell}$. The first column indicates the leptonic invariant mass bin for which the quantities in the subsequent columns are reported. The last column reports the ratio $\frac{\sigma_{\ell\ell}}{\sigma_{Z^*}}$, which is defined as:

$$\frac{\sigma_{\ell\ell}}{\sigma_{Z^*}} = \frac{\sigma_{NLO}^{Z\ell\ell\ell\bar{\ell}} + \sigma_{LO}^{gg\rightarrow Z\ell\ell\ell\bar{\ell}}}{\sigma_{NLO}^{gg\rightarrow Z\ell\ell\ell\bar{\ell}}},$$  

The ratio defined above depends weakly on the invariant mass of the leptonic system. The increase of the ratio is partially induced by the enhancement of the relative contribution of the $gg \rightarrow ZZ$ process. In the first row the relative contribution of $gg \rightarrow ZZ$ to the total $ZZ$ cross-section is 13% and it grows to 17% in the last row. This is linked to the choice of scale implemented here, that could be regarded as unnaturally small for large values of the leptonic invariant mass. When the scales are chosen equal to the leptonic invariant mass the ratio $\frac{\sigma_{\ell\ell}}{\sigma_{Z^*}}$ is stable in the range $250 < m_{N\ell} < 1000$ GeV to better than 5%.

4 Pseudorapidity is defined as $\eta = -\log \tan \frac{\theta}{2}$, where $\theta$ is the polar angle of the particle.
Table II shows the scale-driven uncertainties for the quantities considered in Table I. The first sub-columns report the maximum and minimum values of the cross-sections and the ratio \( \frac{\sigma_{\text{miss}}}{\sigma_{\gamma^*}} \) for the scale choice stated above. The scale-driven error on \( \frac{\sigma_{\text{miss}}}{\sigma_{\gamma^*}} \) is dominated by the scale-driven error of the \( gg \rightarrow ZZ \) process.

The higher order QCD corrections to the \( gg \rightarrow ZZ \) process may be large and it is conceivable that they will not be known by the time of the analysis of the first data by the experiments at the LHC. A conservative estimate of the scale-driven error on \( \frac{\sigma_{\text{miss}}}{\sigma_{\gamma^*}} \) could be obtained by multiplying \( \sigma_{\text{LO}} \) by a factor of two while keeping the same relative error as reported in Table II. This would yield a scale error of less than 15\% for \( \frac{\sigma_{\text{miss}}}{\sigma_{\gamma^*}} \).

We have also performed a study of the errors on \( \frac{\sigma_{\text{miss}}^{NLO}}{\sigma_{\gamma^*}} \) and \( \frac{\sigma_{\text{miss}}^{LO}}{\sigma_{\gamma^*}} \) due to the uncertainties in the parton densities, integrating over the mass of the leptonic system to find fractional deviations of 0.5\% and 1.4\% for \( \sqrt{s} = 14 \) TeV, respectively. The \( \sqrt{s} \) dependence of these errors is very weak. The fractional errors of the \( gg \rightarrow ZZ \) cross-sections due to parton density uncertainties is of the order of 5 \( \div \) 10\% after integrating over the mass of the leptonic system, based on studies performed with NLO and LO parton density sets (see Ref. [41] for more details). A detailed study of the parton density error correlations of the ratios \( \frac{\sigma_{\text{miss}}}{\sigma_{\gamma^*}} \) is not performed here.

The experimental errors on \( \frac{\sigma_{\text{miss}}}{\sigma_{\gamma^*}} \) will be dominated by the uncertainties on the lepton identification and isolation efficiencies. These effects cannot be estimated with our parton level study and we leave a systematic investigation of such effects using a parton shower to the experimental collaborations.

The QCD higher order corrections and the relative contribution from the \( gg \rightarrow ZZ \) process to the total ZZ cross-section depend little on the cuts on the lepton \( p_T \). For instance, raising and lowering the lepton \( p_T \) thresholds by 10 GeV results in no significant change in the results. Therefore, the scale errors on the ratio \( \frac{\sigma_{\text{miss}}}{\sigma_{\gamma^*}} \) reported in Table II should hold for similar configurations of leptonic cuts. We have also investigated the stability of the ratio \( \frac{\sigma_{\text{miss}}}{\sigma_{\gamma^*}} \) with \( \sqrt{s} \), in different bins of the mass of the leptonic system (Table III). The results are stable to better than 10\%.

During the early stages of data taking, when the integrated luminosity will be \( \mathcal{O}(100) \) pb\(^{-1}\), only a handful of events are expected to be reconstructed with four isolated leptons. For this scenario the accuracy reported in Table II is sufficient to establish evidence for a significant excess of four lepton events. However, as more data is accumulated a better accuracy will be required and in Section II B we propose the definition of another ratio that could help to further reduce the theoretical uncertainty.

So far we have considered the inclusive production of four leptons without further requirements on the final state. The production of ZZ remains one of the leading backgrounds for searches of four leptons with moderate \( E_{\text{miss}}^T \) [42]. The production of missing transverse momentum in association with ZZ is due to \( \tau \) decays and instrumental \( E_{\text{miss}}^T \). The latter is expected to be mainly due to the mismeasurement of hadronic activity recoiling against the ZZ system and other factors. The \( E_{\text{miss}}^T \) spectrum is driven to a large extent by the transverse momentum of the ZZ system that, in the same spirit as the inclusive cross sections, could be predicted by using the \( p_T \) spectrum of the ZZ. A comparison of the two spectra has been made for \( \sqrt{s} = 14 \) TeV with the help of the package RESBOS [43], showing that they are very similar \(^5\). This study suggests that the observed \( E_{\text{miss}}^T \) spectrum in \( Z^* \) events could indeed be used to predict the \( E_{\text{miss}}^T \) spectrum of ZZ events.

### B. WW Production

The hadronic production of \( W \) pairs has been considered extensively in the literature (for a review, see Ref. [49]). The NLO QCD corrections to \( q\bar{q} \rightarrow WW \) have been presented in Refs. [50, 51], while NLO calculations for \( q\bar{q} \rightarrow 

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\(^5\) This package implements QCD NNLL/NLO order of calculation for \( Z^* \) [44–46] and QCD NLL/NLO order calculation for ZZ production [47, 48]
induced tree-level processes of the type $gg \rightarrow W^+W^-$ of the intermediate invariant masses of the intermediate $W$ bosons in Ref. [59] is used here. We do not take into account gluon-gluon induced tree-level processes of the type $gg \rightarrow WWq\bar{q}$, which have been found to be strongly suppressed in hadronic $WZ$, $W\gamma$ and $Z\gamma$ production [60].

The package MC@F is used for the computation of the cross-sections due to $q\bar{q} \rightarrow WW \rightarrow \ell\ell\nu\nu'$ in NLO QCD, $\sigma_{gg}^{NLO}WW$ [34] and we use the package gg2WW, a parton-level integrator and event generator [59], to compute the $gg \rightarrow W^+W^- \rightarrow \ell\ell\nu\nu'$ cross-sections to leading order, $\sigma_{gg}^{NLO}WW$. As for ZZ production, a complete NNLO QCD description of WW production is not available, and we once again simply sum the cross-sections $\sigma_{NLO}^{WW}$ and $\sigma_{gg}^{NLO}WW$.

We calculate the cross-sections requiring two opposite sign leptons with $p_T > 20$ GeV in the range $|\eta| < 2.5$ with the same $\Delta R$ requirements as in Section II A. It is also required that the modulus of the vector sum of the transverse momenta of the neutrinos be greater than 20 GeV. The Drell-Yan cross-sections are obtained with the same cuts on the leptons as in Section II A. The cross-section for the on-shell $Z$, $\sigma_{NLO}^{WW}$, is obtained by requiring the invariant mass of the lepton pairs be in the range $71 < m_{ll} < 111$ GeV while the cross-section for an off-shell $Z$ corresponds to $m_{ll} > 185$ GeV.

Ratios analogous to Expression 1 are defined for WW and $Z^{(*)}$ production, $\frac{\sigma_{WW}}{\sigma_{Z}}$ and $\frac{\sigma_{WW}}{\sigma_{Z^*}}$. Table IV shows the cross-sections and scale-driven uncertainties for the WW and $Z^{(*)}$ production together with the ratios $\frac{\sigma_{WW}}{\sigma_{Z}}$ and $\frac{\sigma_{WW}}{\sigma_{Z^*}}$.

The maximum deviation for $\sigma_{NLO}^{WW}$ is obtained when allowing both the renormalization and factorization scales to change at the same time, which is not the case for the rest of the processes considered here. The size of the error band for $\frac{\sigma_{WW}}{\sigma_{Z}}$ tends to be larger than that for $\frac{\sigma_{WW}}{\sigma_{Z^*}}$. Estimating higher order corrections by increasing the $gg \rightarrow WW$ cross-section by a factor of two enhances the scale-related fractional deviations of $\frac{\sigma_{WW}}{\sigma_{Z}}$ and $\frac{\sigma_{WW}}{\sigma_{Z^*}}$, although they remain smaller than 15% and 20% respectively.

A detailed study of the errors due to the uncertainties in the parton densities is performed for $\frac{\sigma_{NLO}^{WW}}{\sigma_{Z}}$ and $\frac{\sigma_{NLO}^{WW}}{\sigma_{Z^*}}$, yielding fractional deviations of 1.3% and 0.3% for $\sqrt{s} = 14$ TeV, respectively. The $\sqrt{s}$ dependence of these errors is very weak. A detailed study of the parton density uncertainty correlations of the ratios $\frac{\sigma_{WW}}{\sigma_{Z}}$ and $\frac{\sigma_{WW}}{\sigma_{Z^*}}$ is not performed here. Similarly as for the $gg \rightarrow ZZ$, the fractional errors of the $gg \rightarrow WW$ cross-sections due to parton density uncertainties is of the order of $5 \div 10\%$.

The cross-section ratios reported here correspond to an inclusive event selection, for which the relative contribution of the $gg \rightarrow WW$ diagrams to the total WW cross-section is about 5%. The relative contribution of the $gg \rightarrow WW$ process is significantly larger after the application of cuts for the Higgs boson search [61, 62, 59]. In addition to the expected large QCD higher order correction the scale error of the prediction of $\frac{\sigma_{WW}}{\sigma_{Z}}$ and $\frac{\sigma_{WW}}{\sigma_{Z^*}}$ will be significantly larger than reported in Table IV. An alternative method for predicting the rate of the WW background in the signal-like region for the Higgs boson search was suggested in Ref. [63].

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6 The sum of the transverse momentum of the neutrinos is not equivalent to the measured $E_T^{miss}$. These are a number of factors that, in addition to the detector smearing and other instrumental effects, distort the measurement: limited detector acceptance in $\eta$ and $p_T$, and neutrinos from fragmentation.
The LHC experiments to measure these ratios in addition to the inclusive cross-section measurements.

As anticipated in Section II A, here we consider an additional ratio in order to further suppress the theoretical uncertainties of $\frac{\sigma_{ZZ}}{\sigma_{WW}}$ due to the error on $\sigma_{gg-ZZ}^{LO}$. We evaluate the scale related errors of:

$$\frac{\sigma_{ZZ}}{\sigma_{WW}} = \frac{\sigma_{gg-ZZ}^{NLO} + \sigma_{gg-ZZ}^{LO}}{\sigma_{q\bar{q}-WW}^{NLO} + \sigma_{q\bar{q}-WW}^{LO}}$$

Table V displays the cross-sections $\sigma_{WW}$ and error due to scale variations for $WW$ and $ZZ$ production and the ratio $\frac{\sigma_{WW}}{\sigma_{ZZ}}$, 10² (see text). The event selections specified in Sections II A and II B are applied. The maximum and minimum fractional deviations (see text) are given in %. Results are given for $\sqrt{s} = 14$ TeV.

| $\sigma_{WW}$ | $\delta\sigma_{WW}$ | $\sigma_{ZZ}$ | $\delta\sigma_{ZZ}$ | $\frac{\sigma_{WW}}{\sigma_{ZZ}} \cdot 10^2$ | $\delta\frac{\sigma_{WW}}{\sigma_{ZZ}}$ |
|---------------|---------------------|---------------|---------------------|---------------------------------|------------------|
| 667.0         | 13.9                | 11.51         | 10.9                | 1.73                            | 1.6              |
| -14.4         | -13.1               |               |                     |                                 |                  |

The ratios $\frac{\sigma_{WW}}{\sigma_{ZZ}}$ and $\frac{\sigma_{WW}}{\sigma_{ZZ}}$ are sensitive to the contribution from the $gg \to WW$ diagrams. We strongly encourage the LHC experiments to measure these ratios in addition to the inclusive cross-section measurements.

The production of same sign leptons is of great interest for searches of physics beyond the SM. The process $qq \to W^\pm W^\pm qq$ (that we have not considered above) is one of the leading SM backgrounds, especially for large values of $E_{T}^{miss}$. Nevertheless, a similar ratio $\frac{\sigma_{WW}}{\sigma_{ZZ}}$ could be defined, whose theoretical uncertainties would be dominated by the large error from unknown higher order corrections to the $qq \to W^\pm W^\pm qq$ cross-section [64].

C. ZW Production

The hadronic production of $ZW$ is known to NLO [52, 53] including the leptonic decays. As opposed to the production of $ZZ$ and $WW$, $ZW$ production is not subject to gluon-gluon induced quark loop diagrams and, furthermore, the gluon induced $gg \to ZWq\bar{q}$ contributions are small [60].

The package MCFM is used here for the computation of the cross-sections due to $qq' \to Z^*(\gamma^*)W^\pm \to \ell\ell'\nu\bar{\nu}$ to QCD NLO, $\sigma_{qq' \to ZW}^{NLO}$ [34]. We compute the cross-sections for $ZW$ production requiring three leptons in the range $|y| < 2.5$. For the leading lepton it is required that $p_T > 20$ GeV and the sub-leading leptons have $p_T > 10$ GeV. The same $\Delta R$ cuts as those required in Section II A are applied here. The invariant mass of the leptons from $Z^*(\gamma^*)$ is required to be larger than 20 GeV. It is also required that the $p_T$ of the neutrino be larger than 20 GeV. The cross-sections for $Z^*$ are obtained for $M_{Z^*} > 195$ GeV.

7 The production of same sign leptons form the $t\bar{t}$ decays dominates the production from SM processes of same-sign leptons at low $E_{T}^{miss}$.
Table VI displays the cross-sections for $ZW$ and $Z^*$ and the ratios $\frac{\sigma_{ZW}}{\sigma_{Z^*}} \cdot 10^3$ and $\frac{\sigma_{ZW}}{\sigma_{Z^*}}$ (see text). The nominal cross-sections are given in the second row in fb. Cross-sections for $Z^*$ are given for the range $M_{Z^*} > 195$ GeV. The event selection specified in Section II C is applied. The fractional deviations in the second and third rows are given in %. Results are given for $\sqrt{s} = 14$ TeV.

| $\frac{\sigma_{ZW}}{\sigma_{Z^*}}$ | $\frac{\sigma_{Z^W}}{\sigma_{Z^*}}$ | $\frac{\sigma_{ZW}}{\sigma_{Z^*}} \cdot 10^3$ | $\frac{\sigma_{ZW}}{\sigma_{Z^*}}$ |
|----------------------|----------------------|----------------------|----------------------|
| Nominal              | 1898.4               | 92.5                 | 0.118                |
| Maximum              | 1.6                  | 12.9                 | 16.0                 |
| Minimum              | -9.2                 | -12.0                | -11.3                | -6.8 |

As pointed out in Section I, the requirement of a jet veto is instrumental in separating the multi-lepton production coming from the decays of $VV$ from that of $t\bar{t}$ production. The latter is associated with large hadronic activity and it is strongly suppressed by the application of a veto on high $p_T$ hadronic jets [1–3].

The jet veto survival probability (JVSP, or $\epsilon_{jv}$) is defined as the fraction of the events with leptons passing the analysis requirements that do not display a parton, a quark or a gluon, with a $p_T$ above a certain threshold in the range $|\eta| < 5$ \(^{8}\). Here we attempt to address the possibility of predicting the JVSP for vector boson pairs by using the production of di-leptons from the Drell-Yan mechanism in a similar invariant mass range.

The nominal results for the JVSP are obtained with the QCD NLO ME used in previous sections. No corrections due to detector and hadronization effects are taken into account in the nominal results reported here, although one might expect them to mostly cancel out in the ratio defined here. The impact of multiple gluon radiation will be discussed below. The results in this Section are obtained with the same settings and event selections as those used in Section II.

Tables VII and VIII report results for the JVSP for the $WW$ and $ZW$ production. The central values, $\epsilon_{jv}^{VV}$, $\epsilon_{jv}^{WW}$ and $\epsilon_{jv}^{ZW}$ are reported, together with the maximum and minimum fractional deviations due to the scale variations, expressed as percentages. Results are reported for different values of the parton $p_T$ threshold (in GeV). Results are also shown for the ratios $\frac{\epsilon_{jv}^{WW}}{\epsilon_{jv}^{Z^*}}$ and $\frac{\epsilon_{jv}^{ZW}}{\epsilon_{jv}^{Z^*}}$, quoted for $M_{Z^*} > 185$ GeV and $M_{Z^*} > 195$ GeV, respectively. The maximum deviations reported in Tables VII and VIII for the ratios $\frac{\epsilon_{jv}^{WW}}{\epsilon_{jv}^{Z^*}}$ and $\frac{\epsilon_{jv}^{ZW}}{\epsilon_{jv}^{Z^*}}$ are less than 10% and have a

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\(^{8}\) The application of a jet veto requirement is usually referred to as the full jet veto. This is done to distinguish it from the application of a veto on jets in addition to two well separated jets, usually performed to isolate the Higgs boson produced via Vector Boson Fusion. The latter is not considered in this paper.
TABLE VII: Central values and scale-driven uncertainties of the jet veto survival probability for the $Z^*$ and $WW$ production for different values of the parton $p_T$ threshold (in GeV). For a veto the parton is required to be in the range $|\eta| < 5$. Results for $Z^*$ are given for the range $M_{Z^*} > 185$ GeV. The scale related uncertainty is expressed in %. Results are obtained for $\sqrt{s} = 14$ TeV.

| $p_T$ | $\epsilon_{jv}^Z$ | $\delta \epsilon_{jv}^Z$ | $\epsilon_{WW}^{jv}$ | $\delta \epsilon_{WW}^{jv}$ | $\epsilon_{WW}^{W*(jv)}$ | $\delta \epsilon_{WW}^{W*(jv)}$ |
|-------|------------------|------------------|------------------|------------------|------------------|------------------|
| 20    | 0.67             | 5.5              | 0.52             | 11.9             | 0.78             | 5.1              |
|       | -3.2             | -15.2            | -15.2            | -3.2             |                  |                  |
| 30    | 0.76             | 5.1              | 0.63             | 8.3              | 0.82             | 3.6              |
|       | -7.8             | -9.1             | -9.1             | -2.1             |                  |                  |
| 40    | 0.82             | 3.5              | 0.70             | 6.6              | 0.88             | 3.0              |
|       | -5.3             | -5.9             | -5.9             | -1.9             |                  |                  |
| 50    | 0.86             | 2.9              | 0.75             | 5.5              | 0.87             | 2.6              |
|       | -3.8             | -5.0             | -5.0             | -1.8             |                  |                  |
| 100   | 0.94             | 1.2              | 0.88             | 2.6              | 0.93             | 1.3              |
|       | -1.6             | -2.6             | -2.6             | -1.1             |                  |                  |

The tendency to decrease with increasing $p_T$ threshold. A more precise prediction of this quantity would require the use of the calculation of Drell-Yan and $VV$ production at NNLO. Only the former is available [65–68]. We could note that some steps toward this have already been taken, such as NLO calculations of $WW+\text{jet}$ production [69–71].

The impact on $\epsilon_{jv}^Z$ of final state radiation, hadronization and multiple gluon radiation (by means of the parton shower approximation) are studied with Pythia [72, 73]. The impact of these effects on $\epsilon_{WW}^{jv}$ are studied with the MC@NLO [74] and ALPGEN [75] packages. It is observed that the effect of multiple gluon radiation on the JVSP for parton $p_T$ threshold values in the range $20 < p_T < 30$ GeV is significant. After taking account of the hadron to parton corrections it is observed that the JVSP decreases by about 10% for parton $p_T$ thresholds around 30 GeV.

This effect diminishes as the $p_T$ threshold increases. The impact of this effect on the ratio $\frac{\epsilon_{WW}^{jv}}{\epsilon_{jv}^Z}$ is less than 5% for the same parton $p_T$ threshold, although more detailed studies are required in order to determine the theoretical errors on this correction.

The JVSP is also evaluated for $Z$ events, $\epsilon_{jv}^Z$. The values of $\epsilon_{jv}^Z$ are 13% and 12% greater than $\epsilon_{jv}^Z$ for the values of the parton $p_T$ thresholds of 20 and 30 GeV, respectively. The use of off-shell $Z$ events is preferred to predict the JVSP of $VV$. The use of on-shell $Z$ events for these studies is not precluded, although it would lead to enhanced theoretical errors on the ratios discussed here.

The values of $\epsilon_{WW}^{jv}$ reported here do not include the contribution from the gluon-gluon initiated processes discussed above since they do not include any radiation upon which to veto. A calculation of the rate of $gg \rightarrow WW$ would therefore greatly improve the estimates of the quantity $\epsilon_{WW}^{jv}$ given here Assuming that the relative rate $gg \rightarrow WW$ with respect to the total $WW$ rate is double that reported in Table IV, the maximum and minimum possible fractional deviations of $\epsilon_{WW}^{jv}$ would be about 5% and -9% for the parton $p_T$ threshold of 30 GeV, respectively. These correspond to unphysical extreme cases when the JVSP for the $gg \rightarrow WW$ process is assumed to be 100 and 0%, respectively. It is important to note that these statements are applicable only to event selections similar to the ones chosen in this paper.

It is important to note that selecting off-shell $Z$ bosons in association with at least one high $p_T$ jet requires to subtract $t\bar{t}$ backgrounds. The latter can be suppressed by the application of an $E_T^{\text{miss}}$ cut not pointing in the direction of the lead jet in the event. Further studies are required to address the contamination of $t\bar{t}$ backgrounds. In order to circumvent this issue the ratio of the expected rate for Drell-Yan events to that of $VV$ after a jet veto can be defined. The errors on these ratios are similar to those of the ratios reported in this Section.

The ability to control the JVSP for $VV$ production gives us a powerful handle to understand better the interplay between this and related $t\bar{t}$ backgrounds. The residual contribution of $t\bar{t}$ events after the application of a jet veto can be evaluated by extrapolation after subtracting for the contribution of $VV$ production. This technique and the study of the corresponding theoretical errors will be developed further in the future.

A change in the $|\eta|$ bound from 5 to 3 does not change the JVSP of $VV$ considerably, as most of the partons lie in the range $|\eta| < 3$. The reconstruction of hadronic jets in the range $3 < |\eta| < 5$ is more challenging than in the central regions of the detector and we therefore consider the possibility of relaxing the requirement $|\eta| < 5$ used by the experiments. This would also be appropriate for the early stages of data taking. The LO matrix elements for $t\bar{t}$ and $t\bar{t}j$ available in MCFM are used for the evaluation of the JVSP for the $t\bar{t}$ processes, using the event selection described in Section IIIB. The JVSP for the $t\bar{t}$ ($0j$) and $t\bar{t}j$ production increases by 26% and 56% for a parton $p_T$
TABLE VIII: Central values and scale-driven uncertainty of the jet veto survival probability for the $Z^*$ and $ZW$ production for different values of the parton $p_T$ threshold (in GeV). For a veto the parton is required to be the range $|\eta| < 5$. Results for $Z^*$ are given for the range $M_{Z^*} > 195$ GeV. The scale-driven uncertainty is expressed in %. Results are obtained for $\sqrt{s} = 14$ TeV.

| $p_T$ | $\epsilon_{jv}^{Z^*}$ | $\delta \epsilon_{jv}^{Z^*}$ | $\epsilon_{jv}^{ZW}$ | $\delta \epsilon_{jv}^{ZW}$ | $\epsilon_{jv}^{Z^*}$ | $\delta \epsilon_{jv}^{Z^*}$ |
|-------|----------------|-----------------|-----------------|-----------------|----------------|-----------------|
| 20    | 0.67           | 8.5             | 0.48            | 13.2            | 0.71           | 6.3             |
|       | -13.2          |                 | -15.3           |                 | -7.3           |                 |
| 30    | 0.76           | 5.1             | 0.57            | 9.7             | 0.75           | 5.0             |
|       | -7.8           |                 | -10.8           |                 | -5.9           |                 |
| 40    | 0.82           | 3.5             | 0.64            | 7.7             | 0.78           | 4.0             |
|       | -5.3           |                 | -9.2            |                 | -5.3           |                 |
| 50    | 0.86           | 2.9             | 0.68            | 6.5             | 0.80           | 3.5             |
|       | -3.8           |                 | -7.8            |                 | -4.7           |                 |
| 100   | 0.94           | 1.2             | 0.82            | 3.6             | 0.87           | 2.3             |
|       | -1.6           |                 | -4.6            |                 | -3.0           |                 |

TABLE IX: The dependence of various jet related variables of $WW$ and $Z^*$ production on the center of mass energy of proton-proton collision (in TeV). Results for the central jet veto survival probability are given for a $p_T$ threshold of 30 GeV.

| $\sqrt{s}$ | $< p_T >$ | $< |\eta| >$ | $\epsilon_{jv}$ | $< p_T >$ | $< |\eta| >$ | $\epsilon_{jv}$ |
|------------|-----------|-------------|-----------------|-----------|-------------|-----------------|
| $WW$       |           |             |                 | $ZW$      |             |                 |
| 14         | 42.0      | 0.78        | 0.63            | 23.9      | 0.58        | 0.76            |
| 10         | 34.6      | 0.68        | 0.68            | 21.0      | 0.53        | 0.78            |
| 8          | 30.1      | 0.62        | 0.71            | 18.1      | 0.47        | 0.81            |

threshold of 30 GeV $^9$. These results represent a mild increase of the overall background contributions in analyses with a tight jet veto.

The $\sqrt{s}$ dependence of the main hadronic variables and the JVSP are studied for $WW$ and $Z^*$ production. Table IX displays the $\sqrt{s}$ evolution of the average $p_T$ (in GeV) and $|\eta|$ of the parton. As expected from the perturbative analysis, the $p_T$ of the parton decreases with decreasing $\sqrt{s}$. As $\sqrt{s}$ decreases the longitudinal boost of particles produced in the hard scattering of the proton-proton collision decreases, which is reflected by the decrease of the average parton $|\eta|$. The increase of the average parton $p_T$ and decrease of the parton $|\eta|$ as $\sqrt{s}$ decreases are two competing effects as far as the JVSP is concerned. Table IX shows $\epsilon_{jv}^{WW}$, $\epsilon_{jv}^{Z^*}$ and $\epsilon_{jv}^{Z^*}$ (calculated for a $p_T$ threshold of 30 GeV) as a function of $\sqrt{s}$. Overall, the JVSP increases mildly as $\sqrt{s}$ decreases. The ratio $\frac{\epsilon_{jv}^{Z^*}}{\epsilon_{jv}^{WW}}$ is even more stable, varying by less than 10% in the rate $6 < \sqrt{s} < 14$ TeV. The same discussion applies to the JVSP for the $ZW$ production. The errors reported in Tables VII and VIII have also been studied as a function of $\sqrt{s}$. The errors due to scale variations in $\epsilon_{jv}^{WW}$ and $\epsilon_{jv}^{Z^*}$ have a tendency to increase, while remaining smaller than 10%. The JVSP increases by 8% and 4% for $WW$ and $Z^*$, respectively, when going from $\sqrt{s} = 14$ TeV to $\sqrt{s} = 10$ TeV. The ratio $\frac{\epsilon_{jv}^{WW}}{\epsilon_{jv}^{Z^*}}$ is even more stable with $\sqrt{s}$.

As shown in Table IX, the fraction of partons in the range $|\eta| < 3$ increases as $\sqrt{s}$ decreases. This effect is stronger when considering the $\eta$ distributions of the decay products of the $t\bar{t}$ (0j) and $t\bar{t}j$ production. For instance, the JVSP increases by 18% and 8% for the $t\bar{t}$ (0j) production when relaxing the jet veto $\eta$ range (for a parton $p_T$ threshold of 30 GeV) for $\sqrt{s} = 10$ and 6 TeV, respectively. This should be compared with 26% for $\sqrt{s} = 14$ TeV. This further motivates relaxing the $|\eta|$ range of the jet veto, especially during the early stages of data taking.

$^9$ It is important to note that the JVSP for the $t\bar{t}j$ production is less than half of that of $t\bar{t}$ (0j) production, indicating that the $t\bar{t}j$ production will play a minor role when considering event selections with a tight full jet veto. This is the case of the Higgs boson search with the $H \to WW$ decay.
We have also studied the JVSP for $ZZ$ production. The rate of production of four leptons inclusively from SM processes is affected little by the decays of $\bar{t}t$. However, $\bar{t}t$, $t\bar{t}t\bar{t}$ and $t\bar{t}Z^*(\gamma^*)$ production contribute considerably in final states with large $E_\text{miss}^{\text{miss}}$ [42]. The application of a jet veto could be a viable option to suppress these backgrounds, for which it is necessary to understand the JVSP for $ZZ$ production. The JVSP for $ZZ$ production is considerably closer to $\epsilon_{\text{jet}}^{ZZ}$ than that of $WW$ production. The ratio $\frac{\epsilon_{\text{jet}}^{ZZ}}{\epsilon_{\text{jet}}^{WW}}$ is equal to 0.92, 0.93 and 0.95 for $\sqrt{s} = 14, 10$ and 8 TeV, respectively. The errors due to the scale variations are very similar to those reported in Table VII.

IV. CONCLUSIONS

The search for new physics in final states with multiple charged leptons and $E_\text{miss}^{\text{miss}}$ carried by neutrinos or other particles escaping detection is arguably one of most the interesting among the feasible signatures at the LHC. The production of two weak bosons will be one of the most important sources of SM backgrounds for these final states. In this paper we consider several quantities that can help normalize rates for the production of weak boson pairs. Ratios involving the production of two weak bosons and Drell-Yan are investigated and the corresponding theoretical errors are evaluated. We consider ratios of inclusive cross-sections of $VV$ to that of the Drell-Yan process. We include the production of $WW$ and $ZZ$ through gluon-gluon fusion at order $O(\alpha_s^2)$. We have considered the use of both on-shell and off-shell $Z$ production. We find that the use of off-shell $Z$ production tends to result in smaller errors due to scale variations and parton density uncertainties, depending on the ratio. We also consider the ratio of the cross-section for $ZZ$ to that for $WW$ production as an additional handle to reduce the theoretical errors on the prediction of the $ZZ$ cross-section. We strongly encourage the CMS and ATLAS experiments to measure the ratio of the $WW$ cross-section to that of the $Z$ production.

The possibility of predicting the jet veto survival probability of $VV$ production with Drell-Yan is also considered. The use of off-shell $Z$ events is preferred for the prediction of the JVSP of $VV$ production. Our studies indicate that reducing the $\eta$ range of the jet veto used to suppress $\bar{t}t$ backgrounds is well motivated.

Overall, the theoretical errors on the quantities presented here are less than $5 \pm 20\%$. Moreover, their dependence on the center of mass energy of the proton-proton collision is weak, so that early measurements at lower energies may help guide later more detailed studies.

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