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ACCURACY ASSESSMENT OF AIRCRAFT POSITIONING USING THE DUAL-FREQUENCY GPS CODE OBSERVATIONS IN AVIATION

This study publishes results of tests with regard to determination of the aircraft positioning accuracy by means of the GPS navigation in aviation. The research exploits the mathematical model of the linear combination "Ionosphere-Free" in order to designate the coordinates of an aircraft. The research uses the actual GPS code observations, recorded by a satellite receiver mounted in the Cessna 172, at the time of the experiment for the EPDE military aerodrome in Dęblin. The computations of the position of the Cessna 172 aircraft for the linear combination "Ionosphere-Free" were made in the APS Toolbox v.1.0.0 programme. Within evaluation of accuracy of the GPS positioning in aviation, the determined coordinates of the aircraft Cessna 172 from the APS programme were compared to an accurate reference position from the solution derived by the PPP measurement technique. In the research, the authors obtained an average positioning accuracy of approximately 5 m in the geocentric XYZ coordinates and approximately 4 m in the ellipsoidal BLh coordinates. In addition, the 3D-error parameter is lower than 7 m for the XYZ geocentric coordinates.

Keywords: GPS, Ionosphere-Free linear combination, accuracy, PPP method, aviation

1 Introduction

In the 21st century, the GNSS satellite technology became a common method of aircraft positioning in the field of air navigation and air transport. Development of modern GNSS global navigation systems, such as GPS, GLONASS, BeiDou, Galileo, and augmentation systems SBAS (EGNOS, SDCM, WAAS, MSAS, GAGAN, NAVIC) enabled their full operation and implementation in the process of determining the aircraft position. The framework of application, operation and implementation of the GNSS satellite technology in aviation has been clearly defined by the International Civil Aviation Organization (ICAO). The Annex 10 to the Chicago Convention currently allows the use of the GNSS satellite technique in aviation for the needs of performing air operations within the navigation systems of: GPS and GLONASS as GNSS satellite systems which are certified by the ICAO and augmentation systems: ABAS, SBAS, GBAS [1-3].

In the case of the global GNSS navigation systems, only the GPS and GLONASS satellite systems are certified for a general use in civil aviation. It should be emphasized that the GPS and GLONASS systems are fully operational and provide continuous satellite positioning for its users across the globe for 24 hours a day. Certification of the GPS and GLONASS navigation systems in civil aviation includes such parameters as accuracy, availability, reliability and continuity [4]. In accordance with the ICAO recommendation, the accuracy of determining the position of an aircraft with the use of the GPS navigation system must not exceed 17 m for navigation in the horizontal plane, and 37 m for navigation in the vertical plane [5]. Furthermore, the time synchronization error in the GPS system during a flight operation must not be worse than 40 ns (approximately 12 m). In addition, error of the GPS satellite's position in the orbit must not be greater than 30 m, whereas an error of determining the GPS satellite speed and acceleration must not exceed values of 0.006 m/s and 0.002 m/s², respectively. In turn, availability of the constellation of the GPS satellites during the flight operations should exceed 90%. The credibility parameter of the GPS system functioning in the civil aviation should exceed 99.70% across the whole globe. The likelihood of the lack of continuity of the navigation solution of an aircraft position by means of the GPS observation must not exceed 2·10⁻⁶ per hour [6]. It should be mentioned that the criteria of the parameters of accuracy, availability, reliability and continuity are referenced to the standard SPS positioning service in the GPS navigation system [7]. Within the Standard Positioning Service, it is possible to use L1-C/A observation codes to determine the coordinates of an aircraft in the GPS system. It must be noted that the GPS satellites transmit the signal L1-C/A on the carrier frequency of 1575.42 MHz, using the code-division multiple access technique (CDMA) [8].

The main aim of this article is to determine the positioning accuracy of the aircraft Cessna 172 based on the GPS solution. An analysis of the accuracy of the aircraft positioning was carried out based on the actual navigation data from the GPS satellite system, registered by an airborne receiver Topcon HiperPro, mounted in an aircraft Cessna 172. The position of the Cessna 172 was...
The fundamental observation equation of the linear combination Ionosphere-Free, which facilitates the possibility of determining an aircraft position in the GPS satellite system, can be expressed as [9]:

$$ P_i = \alpha_i P_1 + \alpha_2 P_2 = d + c (dtr - ds) + Trop + Rel + M_{ps}, \quad (1) $$

where:
- $P_i$ - the “Ionosphere-Free” linear combination for the GPS code observations,
- $(\alpha_1, \alpha_2)$ - linear coefficients,
- $(P_1, P_2)$ - code observations at the 1st and 2nd frequency in the GPS system,
- $d$ - geometric distance between satellite and receiver,
- $d = \sqrt{(x - X_s)^2 + (y - Y_s)^2 + (z - Z_s)^2},$
- $(x,y,z)$ - coordinates of the aircraft in XYZ geocentric frame,
- $(X_s,Y_s,Z_s)$ - satellite coordinates in GPS system,
- $c$ - light speed,
- $dtr$ - receiver clock bias correction,
- $ds$ - satellite clock bias correction,
- $Trop$ - tropospheric delay,
- $Rel$ - relativistic effect,
- $M_{ps}$ - multipath effect for the GPS code observations.

Coordinates of the aircraft from Equation (1) are determined using the least squares method in a stochastic model, as [10]:

$$ \begin{align*}
Q &= N^{-1} L \\
A &= 1 + \frac{d_{11}}{d_{21}} \\
B &= \frac{d_{22}}{d_{21}} \\
C &= \frac{d_{33}}{d_{21}} \end{align*} $$

Equation (2)

$$ \begin{align*}
Q &= N^{-1} L \\
A &= 1 + \frac{d_{11}}{d_{21}} \\
B &= \frac{d_{22}}{d_{21}} \\
C &= \frac{d_{33}}{d_{21}} \end{align*} $$

where:
- $Q$ - vector with unknown parameters,
- $N = A^T \cdot p \cdot A$ - matrix of the normal equations frame,
- $A$ - matrix of coefficients, matrix is full rank,
- $p$ - matrix of weights,
- $L = A^T \cdot p \cdot dl$ - vector of absolute terms,
- $dl$ - vector with difference between measurements and modeled parameters,
- $v$ - vector of residuals.

The determined aircraft coordinates from Equations (1) and (2) are physically referenced to the geocentric XYZ frame. Alternatively, there is a possibility to express aircraft coordinates in the ellipsoidal BLh frame. In this case, it is necessary to use a transformation between the geocentric XYZ frame and the ellipsoidal BLh frame in iterative solution, as shown below [11]:

$$ B = \arctan \left( \frac{z}{p} + \frac{\delta_1}{\sqrt{\delta_2 + \delta_3}} \right), $$

$$ L = \arctan \left( \frac{\gamma}{\chi} \right); \quad h = \frac{p}{\cos B} - R, $$

where:
- $(a,b)$ - semi-major and semi-minor axes of the ellipsoid frame, respectively,
- $\varepsilon$ - eccentricity, $\varepsilon = \sqrt{\frac{a^2 - b^2}{a^2}},$
- $R$ - radius of curvature of the prime vertical,
- $R = \frac{a}{\sqrt{1 - \varepsilon^2 \sin^2 B}},$
- $\rho = \frac{a}{\varepsilon \sqrt{1 - \varepsilon^2}},$
- $\delta_1 = \frac{a \cdot e}{\rho \sqrt{1 - \varepsilon^2}},$
- $\delta_2 = \frac{1}{1 - \varepsilon^2},$
- $i - 1$ - previous iteration,
- $(B,L,h)$ - geodetic coordinates of aircraft’s position,
- $B$ - Latitude,
- $L$ - Longitude,
- $h$ - ellipsoidal height.

3 Research experiment

The numerical tests for the presented research method were performed for the actual navigation and GPS observation data, obtained from the airborne Topcon HiperPro receiver, mounted in an aircraft Cessna 172. The test flight by the Cessna 172 was executed over the military airport EPDE, in Dęblin. Duration of the flight was approximately one hour, with the maximum speed of the flight reaching 80 m/s. The geodetic Topcon HiperPro receiver worked in the kinematic mode, gathering the GPS data at a frequency of 1 s. In order to reduce the effect of multipath interference and radio disturbances, the Topcon HiperPro receiver was installed in the cockpit just behind the plexiglass. The GPS code observations, stored in the memory card of the geodetic receiver Topcon HiperPro, were used to reproduce the position of the aircraft Cessna 172 in the post-processing mode. The numerical calculations to determine the position of the Cessna 172 were made in the authors’ original software APS (Aircraft Positioning Software) Toolbox v.1.0.0, which was fully developed in the Scilab 6.0.0. environment. For the purpose of the conducted numerical calculations, the configuration of the APS programme was set, as shown in Table 1.

4 Results and discussion

The determined Cessna 172 coordinates in APS programme, in the geocentric XYZ frame and in the ellipsoidal BLh frame, were compared to the actual reference trajectory of the aircraft flight in order to determine the accuracy of the GPS signal in aviation. The precise...
Table 1 Configuration of computations in the APS software

| Parameter                                      | Configuration                                                                 |
|------------------------------------------------|-------------------------------------------------------------------------------|
| GNSS system                                    | GPS system                                                                   |
| type of observations                           | code observations at the 1st and 2nd frequency in GPS system                  |
| type of RINEX file                             | 2.10                                                                          |
| source of satellite ephemeris data             | precise ephemeris from the IGS service                                        |
| source of satellite clock data                 | precise ephemeris from the IGS service                                        |
| method of satellite position computation       | 9-degrees Lagrange polynomial                                                 |
| method of satellite clock bias computation     | 9-degrees Lagrange polynomial                                                 |
| effect of Earth rotation and time of pseudorange travelling through atmosphere | applied                                                                      |
| relativistic effect                            | applied                                                                      |
| troposphere source                             | Simple model                                                                 |
| receiver clock bias                            | estimated                                                                    |
| multipath and measurement noise                | not applied                                                                  |
| satellite and receiver phase center offset     | based on ANTEX file from IGS service                                          |
| Sagnac effect                                  | Applied                                                                      |
| Cut-off elevation                              | 5°                                                                            |
| a priori standard deviation of pseudorange observations | 1 m                                                                        |
| positioning mode                               | kinematic                                                                    |
| mathematical model of solution                 | least square estimation in iterative scheme                                   |
| adjustment processing                          | Applied                                                                      |
| maximum number of iterations in a single measurement epoch | N=10                                                                       |
| number of unknown parameters                   | k=4, for each measurement epoch                                              |
| number of observations                         | n>4, for each measurement epoch                                              |
| interval of computations                       | 1 s                                                                          |
| initial coordinates of aircraft position       | based on header of RINEX file                                                |
| time of the GPS system                         | GPS Time                                                                     |
| reference frame                                | IGS’08                                                                       |
| format of output coordinates                   | geocentric XYZ and ellipsoidal BLh                                           |
| local test of residuals                        | applied                                                                      |
| global statistical test                         | test Chi-square                                                              |
| significance level                             | (1 – α = 0.95)                                                              |
| DOP coefficients                               | estimated                                                                    |
| coefficients value for HPL and VPL level       | k_{HPL} = 6.18 and k_{VPL} = 5.33                                             |

The reference flight trajectory of the Cessna 172 was determined using the PPP precision measurement technique. The PPP measurement technique uses the mathematical model of the linear combination equation - “Ionosphere-Free”. The computations of the reference position of the aircraft Cessna 172 for the PPP measurement technique were made in the CSRS-PPP programme [12]. In the framework of the calculations performed in the CSRS-PPP programme, the authors used dual frequency P1/P2 code and L1/L2 phase observations from the airborne receiver Topcon HiperPro. The CSRS-PPP programme uses the IGS precise products such as SP3 precise ephemeris, precise satellite clocks CLK, the characteristics of the antenna phase center of the satellite/receiver ANTEX file format, and DCB hardware delay file format for the computations. The position of the Cessna 172 in the CSRS-PPP programme is expressed in the geocentric XYZ, as well as ellipsoid BLh coordinates, in the global frame IGS’08, whereas the scale of the reference time is the GPS Time. It is worth adding that the program CSRS-PPP allows an accurate determination of kinematic positioning for the aircraft with mean errors of coordinates at a level of approximately 10 cm [13].

Accuracy of the GPS code positioning for the presented research method in the APS programme was defined both in the geocentric XYZ coordinate frame and in the ellipsoidal BLh frame. The accuracy of the GPS positioning in geocentric XYZ coordinates is specified as [14]:
the RMS error along the axis Z is equal to 1.9 m. The span of the GPS positioning accuracy along the X axis is over 17.5 m, along the Y axis it is approximately 6 m, and along the Z axis it is over 15 m. It is worth noting that approximately 75% of the accuracy of GPS positioning results along the X axis are less than 0. On the other hand, approximately 97% results of the GPS positioning accuracy along the axis Y is less than 0. Moreover, approximately 99% results of the GPS positioning accuracy along the axis Z is less than 0. It can therefore be concluded that results obtained with regard to accuracy of the GPS positioning in the APS programme are lower than the readings of the aircraft Cessna 172 position in the PPP solutions in the CSRS-PPP programme.

Figure 2 shows another parameter of accuracy of the GPS positioning in the geocentric XYZ frame, in the form of the 3D-error. The 3D-error parameter specifies a shift in coordinates of the aircraft Cessna 172 between a solution in the APS programme and in the CSRS-PPP programme in the geocentric XYZ frame. The mathematical formula specifying the value of the 3D-error parameter can be determined as [15]:

\[ 3D - error = \sqrt{(dx)^2 + (dy)^2 + (dz)^2} \]  

Based on the obtained results, it is possible to observe that the value of the 3D-error parameter ranges from 1.2 m to 16.1 m. In addition, the average value of the 3D-error parameter equals 6.9 m. It is worth stressing that the value of the 3D-error parameter towards the end of the observation time decreases to a level below 10 m. The drop in the numerical value of the 3D-error parameter is relevant since it directly translates into the location of the aircraft in the three-dimensional space.

Figure 3 shows results of the GPS positioning accuracy in the ellipsoidal BLh coordinates for the linear combination “Ionosphere-Free”, based on a solution in the APS programme. The positioning accuracy along the X axis in the GPS system for the receiver Topcon HiperPro ranges from -11.8 m to +5.7 m. In addition, the value of the average positioning accuracy along the X axis in the GPS system equals -2.4 m. Moreover, the RMS error along the X axis is equal to 3.4 m. The positioning accuracy along the Y axis for the Topcon HiperPro receiver ranges from -5.2 m to +0.9 m. In addition, the value of the average positioning accuracy along the Y axis in the GPS system is -2.3 m. Additionally, the RMS error along the Y axis is equal to 1.1 m. The positioning accuracy along the Z axis for the Topcon HiperPro receiver ranges from -13.3 m to +2.9 m. Moreover, the value of the average positioning accuracy along the Z axis in the GPS system is -5.1 m. Furthermore, the RMS error along the axis Z is equal to 1.9 m. The span of the GPS positioning accuracy along the X axis is over 17.5 m, along the Y axis it is approximately 6 m, and along the Z axis it is over 15 m. It is worth noting that approximately 75% of the accuracy of GPS positioning results along the X axis are less than 0. On the other hand, approximately 97% results of the GPS positioning accuracy along the axis Y is less than 0. Moreover, approximately 99% results of the GPS positioning accuracy along the axis Z is less than 0. It can therefore be concluded that results obtained with regard to accuracy of the GPS positioning in the APS programme are lower than the readings of the aircraft Cessna 172 position in the PPP solutions in the CSRS-PPP programme.

Figure 2 shows another parameter of accuracy of the GPS positioning in the geocentric XYZ frame, in the form of the 3D-error. The 3D-error parameter specifies a shift in coordinates of the aircraft Cessna 172 between a solution in the APS programme and in the CSRS-PPP programme in the geocentric XYZ frame. The mathematical formula specifying the value of the 3D-error parameter can be determined as [15]:

\[ 3D - error = \sqrt{(dx)^2 + (dy)^2 + (dz)^2} \]  

Based on the obtained results, it is possible to observe that the value of the 3D-error parameter ranges from 1.2 m to 16.1 m. In addition, the average value of the 3D-error parameter equals 6.9 m. It is worth stressing that the value of the 3D-error parameter towards the end of the observation time decreases to a level below 10 m. The drop in the numerical value of the 3D-error parameter is relevant since it directly translates into the location of the aircraft in the three-dimensional space.

Figure 3 shows results of the GPS positioning accuracy in the ellipsoidal BLh coordinates for the linear combination “Ionosphere-Free”, based on a solution in the APS programme. Accuracy of the GPS positioning in the ellipsoidal BLh coordinates is specified as [16]:

\[ dx = x - x_{PPP} \]
\[ dy = y - y_{PPP} \]
\[ dz = z - z_{PPP} \]  

where:
\( (dx, dy, dz) \) - accuracy of the GPS positioning in the XYZ geocentric coordinate frame,
\( x \) - coordinate of the aircraft along the X axis, determined based on Equation (1),
\( y \) - coordinate of the aircraft along the Y axis, determined based on Equation (1),
\( z \) - coordinate of the aircraft along the Z axis, determined based on Equation (1),
\( x_{PPP} \) - coordinate of the aircraft along the X axis, determined from the PPP measurement technique in the CSRS-PPP programme,
\( y_{PPP} \) - coordinate of the aircraft along the Y axis, determined from the PPP measurement technique in the CSRS-PPP programme,
\( z_{PPP} \) - coordinate of the aircraft along the Z axis, determined from the PPP measurement technique in the CSRS-PPP programme.
The positioning accuracy for the B component in the GPS system for the receiver Topcon HiperPro ranges from -6.8 m to +5.4 m. In addition, the average value of the positioning accuracy along the axis B in the GPS navigation system is +0.6 m. Moreover, the RMS error along the axis B is equal to 2.7 m. The positioning accuracy for the component L, for the receiver Topcon HiperPro, ranges from -4.2 m to +2.2 m. Furthermore, the average value of the positioning accuracy along the axis L in the GPS navigation system equals -1.2 m. In addition, the RMS error along the axis L is equal to 0.9 m. The positioning accuracy, for the component h for the receiver Topcon HiperPro, ranges from -15.1 m to +5.5 m. In addition, the average value of positioning accuracy along the axis h in the GPS navigation system is -4.1 m. Besides, the RMS error, along the axis h, is equal to 3.1 m. It is worth stressing that only 38% of the GPS positioning accuracy findings, along the axis B, are below 0. Therefore, readings of the coordinate B in the APS programme are inflated in relation to results in the programme CSRS-PPP. On the other hand, approximately 90% results of the GPS positioning accuracy along the axis L

\[
(d_B, d_L, d_h) = (B - B_{PPP}, L - L_{PPP}, h - h_{PPP}),
\]

where:
- \((d_B, d_L, d_h)\) - accuracy of the GPS positioning in the ellipsoidal BLh frame,
- \(B\) - coordinate of the aircraft for the B component, determined based on Equation (3),
- \(L\) - coordinate of the aircraft for the L component, determined based on Equation (3),
- \(h\) - coordinate of the aircraft for the h component, determined based on Equation (3),
- \(B_{PPP}\) - coordinate of the aircraft along the B axis, determined by the PPP measurement technique in the CSRS-PPP programme,
- \(L_{PPP}\) - coordinate of the aircraft along the L axis, determined by the PPP measurement technique in the CSRS-PPP programme,
- \(h_{PPP}\) - coordinate of the aircraft along the h axis, determined by the PPP measurement technique in the CSRS-PPP programme.

The positioning accuracy for the B component in the GPS system for the receiver Topcon HiperPro ranges from -6.8 m to +5.4 m. In addition, the average value of the positioning accuracy along the axis B in the GPS navigation system is +0.6 m. Moreover, the RMS error along the axis B is equal to 2.7 m. The positioning accuracy for the component L, for the receiver Topcon HiperPro, ranges from -4.2 m to +2.2 m. Furthermore, the average value of the positioning accuracy along the axis L in the GPS navigation system equals -1.2 m. In addition, the RMS error along the axis L is equal to 0.9 m. The positioning accuracy, for the component h for the receiver Topcon HiperPro, ranges from -15.1 m to +5.5 m. In addition, the average value of positioning accuracy along the axis h in the GPS navigation system is -4.1 m. Besides, the RMS error, along the axis h, is equal to 3.1 m. It is worth stressing that only 38% of the GPS positioning accuracy findings, along the axis B, are below 0. Therefore, readings of the coordinate B in the APS programme are inflated in relation to results in the programme CSRS-PPP. On the other hand, approximately 90% results of the GPS positioning accuracy along the axis L
5 Conclusions

The article presents and describes results of the scientific research on use of the dual-frequency GPS code observations in aircraft positioning. In particular, the study focuses on determination of accuracy of the GPS positioning in air transport. During the research, the authors used a linear combination "Ionosphere-Free" as a mathematical model to determine aircraft coordinates. The source materials for the scientific research used the raw P1/P2 code observations in the GPS system from the Topcon HiperPro receiver. The Topcon HiperPro geodetic receiver was installed on board the Cessna 172, which performed a test flight over the EPDE military airport in Dęblin. The collected code P1/P2 observations in the GPS system allowed performing numerical calculations in order to establish coordinates of the Cessna 172. The numerical calculations of the Cessna 172 position were made in the APS v.1.0.0 software programme. For the purpose of determining the GPS positioning accuracy in aviation, the authors made a comparison of the determined coordinates from the APS reference position of the Cessna 172. The precise flight trajectory of the Cessna 172 was determined based on the PPP measurement technique in the CSRS-PPP programme. Based on computations, it was found that the accuracy of the GPS positioning in aviation is:

- between -13.3 m and +5.7 m in the geocentric XYZ coordinates,
- between -15.1 m and +5.5 m in the ellipsoidal BLh coordinates.

In addition, the accuracy measurements of determining the position in the form of the RMS parameter are as follows:

- less than 3.4 m in the geocentric XYZ coordinates,
- less than 3.1 m in the ellipsoidal BLh coordinates.

The obtained research findings indicate a problem with the low GPS positioning accuracy in aviation. The problem is closely related to the choice of a positioning method presented in this work. The dual-frequency GPS code observations have high measurement noise at the carrier frequency L1 and L2. Moreover, in the case of an application of the dual-frequency GPS code observations in navigation computations, there appears an issue of eliminating an ionospheric delay, which directly affects determination of the horizontal coordinates of an aircraft. The authors plans to conduct research into monitoring the ionospheric status during the air operations in the airspace of Poland. Moreover, in the future additional research is planned aimed at exploiting the GLONASS code observations in aircraft positioning in aviation.

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### Annex - Nomenclature

| The abbreviation | The full name |
|------------------|---------------|
| GLONASS          | Globalnaja Nawigacionnaja Sputnikowaja Sistiema / Global Navigation Satellite System |
| GPS              | Global Positioning System |
| BSSD             | Between Satellite Single Difference |
| ICAO             | International Civil Aviation Organization |
| GNSS             | Global Navigation Satellite System |
| ABAS             | Aircraft Based Augmentation System |
| SBAS             | Satellite Based Augmentation System |
| GBAS             | Ground Based Augmentation System |
| EPDE             | ICAO airport code |
| APS              | Aircraft Positioning Software |
| IGS              | International GNSS Service |
| ANTEX            | Antenna Exchange Format |
| RINEX            | Receiver Independent Exchange System |
| HPL              | Horizontal Protection Level |
| VPL              | Vertical Protection Level |
| DOP              | Dilution of Precision |
| MRSE             | Mean Radial Spherical Error |
| PPP              | Precise Point Positioning |
| XYZ              | Geocentric coordinates |
| BLh              | Latitude, Longitude, ellipsoidal height |
| Beidou           | Chinese satellite navigation system |
| Galileo          | European satellite navigation system |
| QZSS             | Japanese regional satellite navigation system |
| EGNOS            | European Geostationary Navigation Overlay Service |
| SDCM             | The System for Differential Corrections and Monitoring |
| WAAS             | The Wide Area Augmentation System |
| MSAS             | The Multi-functional Satellite Augmentation System |
| GAGAN            | The GPS Aided Geo Augmented Navigation |
| NAVIC            | Indian Regional Navigational Satellite System |
| SPS              | Standard Positioning Service |
| C/A              | Coarse Acquisition |
| CDMA             | Code-Division Multiple Access |
| CSRS-PPP         | Canadian Spatial Reference System - Precise Point Positioning |
| DCB              | Differential Code Biases |
| RMS              | Root Mean Square |