DECELERATION IN THE EXPANSION OF SN 1993J

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ABSTRACT

A rarity among supernova, SN 1993J in M81 can be studied with high spatial resolution. Its radio power and distance permit VLBI observations to monitor the expansion of its angular structure. This radio structure was previously revealed to be shell-like and to be undergoing a self-similar expansion at a constant rate. From VLBI observations at wavelengths of 3.6 and 6 cm in the period 6–42 months after explosion, we have discovered that the expansion is decelerating. Our measurement of this deceleration yields estimates of the density profiles of the supernova ejecta and circumstellar material in standard supernova explosion models.

Subject headings: circumstellar matter — galaxies: individual (NGC 3031, M81) — radio continuum: stars — supernovae: individual (SN 1993J) — techniques: interferometric

1 INTRODUCTION

Supernova SN 1993J in M81, discovered by Francisco García of Lugo, Spain (Ripero & García 1993), is a Type Ib supernova (SN) whose red giant progenitor probably had a mass of 12–16 \( M_\odot \) while on the main sequence; at the time of the explosion, \( 3–5 M_\odot \) likely remained in the He core and \( \lesssim 1 M_\odot \) in the He/H envelope (Filippenko, Matheson, & Ho 1993; Shigeyama et al. 1994; Woosley et al. 1994; Iwamoto et al. 1997). The first maximum in the SN optical light curve has been attributed to shock heating of the thin envelope and the second to radioactive decay of \(^{56}\)Co (Nomoto et al. 1993; Shigeyama et al. 1994; Woosley et al. 1994). Modeling of the X-ray emission (Suzuki & Nomoto 1995) also implies an envelope of relatively low mass due to interaction with a binary companion (Nomoto et al. 1993; Woosley et al. 1994).

The standard circumstellar interaction model—hereafter, standard model, or SM—for radio SNe (Chevalier 1996, and references therein) suggests that the radio emission arises from a shocked region between the SN ejecta and the circumstellar material (CSM) that results from the wind of the SN’s progenitor star. More specifically, the SM considers SN ejecta with steep density profiles \( (\rho_0 \propto r^{-2}) \) shocked by a reverse shock that moves inward from the contact surface and a CSM with density profile \( \rho_{\text{csm}} \propto r^{-\gamma} \) shocked by a forward shock that moves outward from the contact surface \( (\gamma = 2 \) corresponds to a steady wind). For \( \gamma > 2 \), self-similar solutions are possible (Chevalier 1982a); the radii of the discontinuity surface, forward shock, and reverse shock are then related, and all evolve in time with the power law \( R \propto t^m \), where \( m \) is a constant that depends on the density profiles of the SN ejecta and CSM.

In our 6 cm VLBI observations of SN 1993J, global arrays formed by the phased VLA antennas in Effelsberg (Germany) and Medicina and Noto (Italy), and various subsets of the 10 antenna VLBA were used. For the first three epochs (see Table 1) Mk IIIA instrumentation and a recording bandwidth of 56 MHz were used, and the data were correlated at the Max-Planck-Institut für Radioastronomie in Bonn, Germany. For the last four epochs, VLBA instrumentation and a recording bandwidth of 64 MHz were used, and the data were correlated at the National Radio Astronomy Observatory in Socorro, NM. The sources 0917+624 and 0954+658 and the nucleus of M81 were observed as calibrators, the first two as

2 OBSERVATIONS AND RESULTS

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amplitude calibrators and the nucleus of M81 both as an amplitude calibrator and, for epochs later than 1996 June, as a phase calibrator. In all cases we analyzed the data using DIFMAP (Shepherd, Pearson, & Taylor 1994) in a standard way, using measured system temperatures and either antenna-temperature measurements or gain-curve information from each antenna as initial calibration. For 0917+624, we obtained brightness maps using self-calibration and the source structure determined by Standke et al. (1996) as an initial model. The calibration correction factors obtained with the self-calibration of 0917+624 were then applied to calibrate the data of SN 1993J and the nucleus of M81. A similar iteration was carried out using the very compact VLBI nucleus of M81, and those new calibration corrections were also applied to the calibration of the data of SN 1993J.

We constructed a map of SN 1993J for each epoch, using a standard process. We used each of the following initial models: a point source, a scaled model from a previous epoch, and a supersymmetrized scaled model (obtained by rotating the scaled model by $n$, such that $360/n$ is an integer, then rotating by $2n$, etc., adding all the rotated models, and rescaling the resulting flux density distribution). The total flux density in each map was checked against the light curve of Van Dyk et al. (1994) and recent VLA measurements. Agreement was found to be better than 5%, except for two epochs in which the discrepancy was as large as 8%. The resultant maps were virtually independent of the starting model and are shown in Figure 1 (Plate L2). For this display, circular convolving beams with sizes proportional to the number of days elapsed since the explosion were used (see Table 1). Such beams permit both a better visualization of the self-similar expansion (the radio structure remains virtually constant except for a time-dependent scale factor) and a better estimate of the deceleration parameter, $m$. In Figure 2 we show the map from the latest epoch (1996 October 22) convolved with an elliptical Gaussian beam whose half-power size is given by the corresponding size of the main lobe of the interferometric beam from that epoch, so that the details of the source structure are more visible than in Figure 1.

Each map of SN 1993J shows a shell-like radio source. The inferred source size depends on how the map is constructed and how it is measured. Because of the non-point-like size of the VLBI beam, a positive bias is introduced in the size estimate of each map: the estimated size is larger than the true size. The fractional bias will systematically decrease for a source increasing in size if the same beam applies for all observations. If uncorrected, this bias introduces a bias in the estimate of the growth rate of the source. However, for self-similar expansion, as here, a method can be found (see below) such that the bias can be kept approximately constant.

### Table 1: SN 1993J Sizes

| Date of Observation | Age (days) | $\lambda$ (cm) | Flux Density (mJy) | VLBI Beam (mas) | Convolution Beam (mas) | Shell Outer Radius (mas) |
|---------------------|------------|----------------|-------------------|----------------|------------------------|-------------------------|
| 1993 Sep 26         | 182        | 3.6            | 78.5              | 0.55 ± 0.46 (176) | 0.26                    | 464 ± 90               |
| 1993 Nov 22         | 239        | 3.6            | 57.3              | 0.52 ± 0.45 (97)   | 0.34                    | 612 ± 22               |
| 1994 Feb 20         | 330        | 3.6            | 51.0              | 0.53 ± 0.44 (65)   | 0.46                    | 824 ± 90               |
| 1994 May 29         | 427        | 3.6            | 41.5              | 0.61 ± 0.52 (257)  | 0.60                    | 1071 ± 28              |
| 1994 Sep 20         | 541        | 6              | 53.4              | 0.69 ± 0.82 (472)  | 0.76                    | 1202 ± 30              |
| 1995 Feb 23         | 607        | 6              | 44.3              | 1.11 ± 0.77 (172)  | 0.98                    | 1567 ± 33              |
| 1995 May 11         | 774        | 6              | 41.8              | 1.22 ± 0.88 (180)  | 1.09                    | 1701 ± 39              |
| 1995 Oct 1          | 917        | 6              | 32.2              | 1.57 ± 1.24 (−270) | 1.29                    | 2026 ± 55              |
| 1996 Mar 28         | 1096       | 6              | 31.3              | 1.58 ± 1.23 (−58)  | 1.54                    | 2501 ± 72              |
| 1996 Jun 17         | 1177       | 6              | 26.5              | 1.37 ± 1.11 (30)   | 1.65                    | 2414 ± 102             |
| 1996 Oct 22         | 1304       | 6              | 26.1              | 1.20 ± 0.97 (−6)   | 1.83                    | 2639 ± 100             |

*Note:* The 3.6 cm observations were reported by Marcaide et al. (1995b), but the data have been reanalyzed and the shell outer radius reestimated in a way similar to that used for the 6 cm data, as described in the text.

a Total flux density used for mapping.

b Major axis × minor axis (position angle) of elliptical Gaussian beam.

c As explained in text.

d Quoted errors are the estimated 1σ.
with source growth and hence does not significantly affect the estimate of the deceleration parameter.

If the shape of the expanding source does not change and the expansion rate is nearly constant, we can largely avoid introducing a spurious deceleration by using a beam size proportional to the number of days between the explosion and the epoch of the source map. Figure 1 (see also Marciaide et al. 1995b) shows that we are indeed in such a situation. An alternate mapping procedure based on using beam sizes proportional to actual source sizes would produce, in principle, a (slight) improvement. In practice, other map errors would probably prevent any discernible improvement.

To use convolving beams as similar as feasible to the VLBI beams and still use the above-described procedure, we chose a range of convolving beam sizes so that each is always within a factor of 2 of its VLBI beam. For the early epochs, we therefore chose small convolving beams and overresolved our images by almost a factor of 2; for the late epochs, we chose large convolving beams and degraded the map resolution by almost a factor of 2. We also applied the same criteria to the 3.6 cm wavelength maps (Marciaide et al. 1995b).

In Table 1, we list the measured outer radius of the SN shell for each epoch of observation and plot the results in Figure 3. Each such size was estimated by the average of the source diameter at the 50% contour level of the map from eight uniformly spread azimuthal cuts through the map. The standard errors quoted in Table 1 result from adding in quadrature an error twice as large as the measurement error in the diameters and an error in determining the 50% contour level location due to map noise and beam size limitations. Using $R \propto t^m$ for the 6 cm data yields $m = 0.89 \pm 0.03$; combining the 3.6 and 6 cm data gives $m = 0.86 \pm 0.02$. Figure 3 shows only the latter result. The reduced $\chi^2$ of the model fit is 0.9; the quoted error has been scaled to correspond to a reduced $\chi^2$ of unity. In contrast, a fit of a straight line ($m = 1$) to the data gives a reduced $\chi^2$ of 6.0.

We find, too, that the better the calibration and the more VLBI observations at a given epoch, the more spherical and smoother the resultant image. Thus, some of the small emission asymmetries in the images may be artifacts.

3. DISCUSSION

Our maps give no indication of any structures developing in the shell by the action of either Raleigh-Taylor instabilities (Chevalier & Blondin 1995) or interaction with the CSM. There is also no evidence of any departure from circularity as suggested by some authors to explain the action of a putative binary companion. We also do not see any emission above $\sim 0.5$ mJy from any compact source at the center of the structure (i.e., a pulsar, as suggested by Woosley et al. 1994 and Shigeyama et al. 1994).

Within the framework of self-similar models, measurement of the time dependence of the attainment of the SN radio emission due to the circumstellar plasma allows us to estimate the exponent of a power-law representation of the density profile of the CSM, for free-free absorption as commonly invoked in radio SN models (Weiler et al. 1996, as references therein), the opacity, $\tau$, is proportional to the density squared integrated along the line of sight. Given a SN radius $R \propto t^m$ and $\rho_{\text{csm}} \propto r^{3m}$, then $\tau \propto t^{3(m-1)/5}$. Van Dyk et al. (1994) found $\tau \propto t^2$ with $m = 0.86 \pm 0.02$, we obtain $s = 1.86^{+0.38}_{-0.16}$ for the homogeneous component of the CSM. Combining this result with $m = 0.86 \pm 0.02$, we obtain $s = 1.66^{+0.38}_{-0.16}$. This value is lower than the $s = 2$ in the SM for a constant stellar wind, but very close to the value $s = 1.7$ given by Fransson, Lundqvist, & Chevalier (1996) to explain the X-ray emission (Zimmermann et al. 1994). Van Dyk et al. (1994) also obtain a similar time dependence for the attenuation of a clumpy medium and hence argue that the clumpy component is spatially distributed in the same way as the homogeneous component. Houck & Fransson (1996) also argue in favor of a clumpy medium on the basis of optical line profiles. Suzuki & Nomoto (1995) postulate CSM with homogeneous and clumpy components to explain X-ray data, but they consider two regions: (1) an inner homogeneous region with a density profile described by $s = 1.7$ out to radii smaller than $\sim 5 \times 10^{19}$ cm and (2) an outer clumpy region with a density profile described by $s = 3$ for the interclump medium at larger radii. Such a model of CSM allows Suzuki & Nomoto (1995) to fit their model to all of the available X-ray data. Specifically, the $s = 3$ clumpy medium is needed to account for the hard X-rays and for part of the H$\alpha$ emission. The SN explosion model of Suzuki & Nomoto (1995), consisting of ejecta and a clumpy CSM as described above, is very different from self-similar models (Chevalier 1982b).

The self-similar case with $m = 0.86$ and $s = 1.66$ gives an ejecta density profile of $n = 11.2^{+0.25}_{-0.19}$. These values correspond to steep profiles, indeed much steeper than the profiles of white dwarfs ($n = 7$) but less steep than those suggested by Baron et al. (1995) from spectral analyses or those used by Suzuki & Nomoto (1995). In the SM for values $n = 11.2$ and $s = 1.66$, the reverse shock radius is $\sim 2\%$ smaller, and the forward shock radius is $\sim 20\%$ larger, than the radius of the contact surface between shocked SN ejecta and shocked CSM (Chevalier 1982b).

Marciaide et al. (1995b) estimate that the width of the radio shell is $\sim 0.3$ times the size of the outer radius (or, equivalently, $\sim 40\%$ of the inner radius). These authors also estimate expansion speeds $\sim 15,000$ km s$^{-1}$, which are compatible with the largest velocities ($\sim 11,000$ km s$^{-1}$) measured in H$\alpha$ (Filippenko, Matheson, & Barth 1994; Patat, Chugai, & Mazzali 1995) if (i) the H$\alpha$ emission originates in the vicinity of the reverse shock, (ii) a homologous expansion is assumed in the ejecta and shocked regions, and (iii) the shock shell is
about twice as large as predicted in the SM. In an attempt to reconcile the SM and the observational results, Houck & Fransson (1996) suggest that clumpy ejecta and/or CSM can broaden the shell. On the other hand, the region of the ejecta shocked by the reverse shock in the model of Suzuki & Nomoto (1995) is even larger than that of the CSM shocked by the forward shock. However, the maximum speeds of the radio outer shell and of the region of Hα emission in the model of Suzuki & Nomoto (1995) match those observed very well, although the density and velocity profiles in the shell are very different from those of the standard model.

If we consider only VLBI results from epochs more than 500 days after the explosion, we obtain $m = 0.89 \pm 0.03$ and $s = 1.62^{+0.13}_{-0.24}$. However, such an age range is in the region in which the Suzuki & Nomoto (1995) model suggests that $s = 3.0$. A contradiction is apparent, and our results therefore argue against their model. Our estimate of $s$ based on that of $m$ is not dependent on a given explosion model but is a determination from the time dependence of the opacity due to an external medium (Weiler et al. 1986; Van Dyk et al. 1994). Furthermore, such time dependence of the opacity has not changed between days 200 and 1000 (S. D. Van Dyk 1997, private communication).

If the physical picture of the radio and Hα emission in the SM were correct, the ~15% decrease in expansion speed measured by VLBI between months 12 and 42 after the explosion would be observable in the Hα emission. On the other hand, if the model of Suzuki & Nomoto (1995) were correct, a decrease in the maximum speed of Hα would not be expected.

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Fig. 1.—Sequences of radio images of supernova SN 1993J at a wavelength of 6 cm placed at vertical positions proportional to the number of days elapsed since explosion. The images clearly show a self-similar expansion. The CLEAN components have been convolved with circular beams whose radii are proportional to the number of days elapsed since explosion (see text). The beam sizes have been chosen so as to be within a factor of 2 of that of the VLBI beam for each observation. Each image in the sequence on the left-hand side has an independent color-coded brightness scale. In the sequence on the right-hand side, the temperature scale is the same for all the images (maximum brightness temperature 8.88 mJy beam$^{-1}$).

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PLATE L2