Extended Version of Reactive Task Allocation and Planning of A Heterogeneous Multi-Robot System

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Abstract—This paper takes the first step towards a reactive, hierarchical multi-robot task allocation and planning framework given a global Linear Temporal Logic specification. In our scenario, legged and wheeled robots collaborate in a heterogeneous team to accomplish a variety of navigation and delivery tasks. However, all robots are susceptible to different types of disturbances including locomotion failures, human interventions, and obstructions from the environment. To address these disturbances, we propose task-level local and global reallocation strategies to efficiently generate updated action-state sequences online while guaranteeing the completion of the original task. In addition, these task reallocation approaches eliminate reconstructing the entire plan or resynthesizing a new task. Lastly, a Behavior Tree execution layer monitors different types of disturbances and employs the reallocation methods to make corresponding recovery strategies. To evaluate this planning framework, dynamic simulations are conducted in a realistic scenario, legged and wheeled robots collaborate in a heterogeneous robot team consisting of quadrupeds and wheeled robots for delivery tasks.

I. INTRODUCTION

Mobile robots have been extensively investigated and deployed in various service applications such as assembly [1], surveillance, [2] and search and rescue [3]. In recent years, quadrupedal robots have been popularized for its superior traversability over unstructured terrains [4]. Nevertheless, even with exceptional locomotion capabilities, legged systems are often unstable, fragile, and less suitable for performing prolonged tasks compared to wheeled robots. However, distinct types of robots can form a heterogeneous team to compensate for their individual disadvantages.

Recent works on multi-robot systems have been focusing on mission planning problems with the assistance of formal languages such as Linear Temporal Logic (LTL) [5]. Originally proposed for model checking [6], LTL is a powerful tool used in the robotics community with a preponderance of research primarily conducted on wheeled robots [7], [8] and legged robots [9]–[11] for task and motion planning. There have also been works [7], [12]–[15] on multi-agent systems, however, objectives are explicitly assigned to individual robots rather than having one global specification. This can be challenging for a large team of robots [16], [17], while in most cases, a global task is simpler to define. Therefore, we propose a simultaneous task allocation and planning (STAP) problem given a global LTL specification.

A line of research exists where STAP problems have been solved with global LTL specifications. In [2], [18] a product model is constructed with an exponential complexity while [19] proposed a team model automaton with a linear complexity, assuming that each robot conducts its task independently. Other works also focused on advanced search algorithms [16], [20], concrete time constraints [21], and collaborative tasks [22]. However, failure recovery during real-world deployment is rarely studied. Meanwhile, single and multi-robot scenarios have been demonstrated with disturbances caused by a change in the environment [23]–[26] or a failure to perform an action [27], but all limited to local LTL specifications. The work of [28] is conceptually similar to our goal, where each robot reallocates its tasks during execution failures, based on a Team Markov Decision Process. However, a set of LTL specifications is provided in advance without identifying the decomposable parts of a global task. Therefore, recovery strategies during the online execution is desirable for STAP problems given global LTL specifications.

In this paper, multiple reallocation approaches subjective to a rich class of online disturbances are proposed to replan on the updated team model given one global LTL specification. A local reallocation efficiently outputs a new action sequence only for the problematic robot, while a global reallocation searches on the entire team model and generates optimal action sequences for all robots. The connection between the high-level reallocation and the low-level disturbance detection is interfaced by a mid-level Behavior Tree (BT). BT is a

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II. PRELIMINARIES

A. LTL BASICS

Linear temporal logic (LTL) has been widely used to encode temporal task specifications and automatically synthesize the system’s transition behaviors. A specification φ is constructed from atomic propositions π ∈ Π, which is evaluated to be True or False and follows the syntax φ := π | ¬φ | φ1 ∧ φ2 | φ1 ∨ φ2 | φ1 U φ2 | φ1 R φ2. Boolean operators “not” and “and” in addition to a set of temporal operators “next”, “until”, and “release”, are denoted. To be concise, we omit the derivations of other boolean operators such as “or”, “implies”, and “if and only if”, as well as temporal operators “eventually” φ and “always” φ.

A common usage of LTL is for constructing an automaton. A non-deterministic automaton (NFA) is defined as a tuple F = (S0, S, δ, F) such that S is a set of states (s0 ∈ S), S ⊆ S is a set of initial states, δ is the input alphabet, and F is a set of accepting states. In addition, LTL formulas are evaluated over a sequence σ : N → 2R where σ(t) ∈ Π represents all true prepositions at time t.

For this framework, a transition system (TS) is created by combining data from the topological map and the robot’s operating states. A TS is defined as a tuple T = (S, s0, A, L) such that S is a set of states (s ∈ S), s0 ∈ S is the initial state, A is a set of available system actions, and L : S → 2R is a labeling function that assigns atomic propositions to states.

Our contributions are summarized as follows:

• A reactive multirobot task allocation and planning framework is proposed to handle disturbances from locomotion failures, pedestrians, and the environment.
• We propose a local and global task reallocation approach based on a team automaton, which eliminates the need to reconstruct the entire team model or resynthesize a new task.
• We present a BT-based execution interface to select between four reactive strategies to address disturbances and failures. Additionally, disturbances can be detected at different rates by leveraging the BT’s modularity property.
• We evaluate our method in a simulated hospital environment with a heterogeneous robot team consisting of both legged and mobile robots as shown in Fig. 1.

B. TASK ALLOCATION

Given the LTL semantics above, a global task φ along with its corresponding NFA F can be specified for a whole team of N agents, each of which has its own TS T and a corresponding PA σ = (S0, Q, δ, F) such that each agent executes its sub-task. The team automaton is a combination of every agent’s PA and all respective TS r such that σT = (S0, Q, δ, F) is the set of initial states, and A = σT ∨ σT ∈ A ∧ σT ∈ δQ(S0, L(σT)).
remaining task to another agent. This special transition is called a switch transition. Therefore, as shown in Fig. 3(a), if a global action sequence $\beta$ on the team automaton is found, we can state that task allocation and planning have been accomplished simultaneously (namely STAP [19]). By projecting $\beta$ onto the PA of each agent, tasks can be executed in parallel. This process of finding an initial set of task sequence is called the offline allocation.

III. PROBLEM FORMULATION

A. Disturbance characterization

In this section, we categorize disturbances into four classes in order to pair a reactive strategy that can efficiently resolve the problem. Unless specified, the following disturbances apply to both legged and wheeled robots.

- **Loss of balance** refers to a scenario where a legged robot falls due to an unstable gait or erratic controller output.
- **Critical failure** refers to an irrecoverable hardware or software malfunction such as a damaged motor or a software glitch.
- **Unexpected robot state change** refers to a situation where a robot detects a sudden shift in the robot’s state.
- **Environmental change** refers to an environmental event preventing the robot from continuing its current task.

B. STAP reallocation

Given the baseline STAP approach (Sec. II), we seek for an efficient reallocation strategy that is specific to each category of disturbance. For this problem, two aspects need to be investigated: 1) a formal guarantee to complete the global task; 2) a set of completed tasks by the whole team. To this end, we define a STAP reallocation problem as the following:

**Problem Statement.** Given an initial task assignment and the current TS of every agent, one finds a set of new action-state sequences for the agents to accomplish the global task without restarting the whole mission or re-synthesizing a new mission.

However, the task reallocation strategies are only compatible with high-level information such as changes in the NFA state or the TS state. Therefore, we propose a BT-based mid-level to organize different disturbance types into comprehensible inputs for the high-level planning framework.

Fig. 2 shows the planning architecture consisting of 1) a high-level task planner that performs offline allocation and online reallocation; 2) a mid-level BT interface to execute the assigned action plan for each agent; 3) low-level controllers that power the actuators on legged and wheeled robots.

IV. REALLOCATION APPROACH

To solve the STAP reallocation problem, we propose two approaches: a local and global approach, both of which are designed at the high level. Fig. 3(b) and 3(c) shows the workflow and conceptual examples of both local and global reallocation.

A. Local reallocation addressing unexpected robot state changes

The offline task allocation process generates an action-state sequence for each agent, which assumes every action is performed successfully. During the execution, however, unexpected interventions could occur, which would undermine the original plan. For instance, if a human removes a load carried by the robot before the robot reaches its destination, an unforeseen robot state change occurs. To resolve this intervention, we introduce the local task reallocation approach. Suppose $\text{Path}^{(r)}$ is a planned state sequence for robot $r$, generated from the original team automaton. Let $\text{Path}^{(r)}(\text{acc})$ denote the agent’s local accepting state and $s^\Delta_T$ be the current state after the intervention. By comparing the state sequence execution history and $\text{Path}^{(r)}$, the last matched state is identified as $\text{Path}^{(r)}(m)$, whose NFA and TS are written as $\text{Path}^{(r)}_Q(m)$ and $\text{Path}^{(r)}_T(m)$. Thus, $\text{Path}^{(r)}_T(m + 1) = s^\Delta_T$. Now, the problem is reformulated to find a path on the local PA, starting from an up-to-date initial set defined as $S^I_{l,p} = \{(r, s_Q, s_T) \in S^I_p | s_T = s^\Delta_T, \forall s_Q \in \delta_Q(\text{Path}^{(r)}_Q(m), L(\text{Path}^{(r)}_T(m)))\}$. Note that the original path can be reused if the current state happens to be on the agent’s original path. This local task reallocation approach is summarized in Algorithm 1. $\text{Path}^{(r)}(i :)$ denotes a sub-path starting from the $i$th element.
Algorithm 1 Local reallocation: unexpected robot state change

Input: \( \mathcal{P}(r), \text{Path}(r) \)
Output: A new path \( \text{Path}(r)^{+} \)

\[
\text{Path}(r)^{+} \leftarrow \text{empty path} \\
\text{Path-set}(r) \leftarrow \text{empty set} \\
\text{for } s \in S_{c}(r) \text{ do} \\
\quad \text{if } s \in \text{Path}(r) \text{ then} \\
\qquad i \leftarrow \text{getIndex(\text{Path}(r)(s))} \\
\qquad \text{Path-set}(r).\text{append(\text{Path}(r)(i :))} \\
\quad \text{else} \\
\qquad \text{Path-set}(r).\text{append(find-path(s,Path(r)(acc)))} \\
\text{end if} \\
\text{end for} \\
\text{Path}(r)^{+} \leftarrow \text{find-best(\text{Path-set}(r))}
\]

Proposition 1. In the presence of one robot experiencing unexpected state changes and all other agents not interfered (i.e., can successfully accomplish their tasks), the global specification \( \phi \) will be fulfilled if a path is found by the local reallocation method in Algorithm 1 on the local PA \( \mathcal{P}(r) \).

Proof. According to Algorithm 1 and the definition of \( S_{c}(r) \), the new state sequence \( \text{Path}(r)^{+} \) (i) connects to agent \( r \)'s executed state sequence through a valid NFA transition since \( s_{Q} \in \delta_{Q}(\text{Path}(r)^{-}(m), \mathcal{L}(\text{Path}(r)^{+}(m)) \); and (ii) ends with the original local accepting state \( \text{Path}(r)(\text{acc}) \). In other words, the originally assigned sub-task for agent \( r \) is fulfilled again. Given the assumption that the rest of the agents are not interfered by any disturbances, agent \( r \)'s newly concatenated sequence, along with the other agents’ planned sequences, consists a global action sequence \( \beta \) on the team automaton \( \mathcal{G} \) again. Then according to the correctness property in [29], the projected global path onto the NFA satisfies the mission specification \( \phi \).

B. Local reallocation addressing transition system changes

In the previous section, the disturbance shifts the robot’s state but does not modify the environment, which will be addressed in this section. Such a disturbance will impact the TS. For instance, if the floor is occupied by an impassable object, the mobile robot would encounter a navigation failure and would not be able to transition to its next expected state. In this case, the robot will receive the changes to be made on TS called \( \text{Info}(t) \). Each update contains three types of information: 1) \( (s_{T}, s_{T}^{\prime}) \in \text{Add}(t) \) if \( s_{T} \) is allowed to transit to \( s_{T}^{\prime} \); 2) \( (s_{T}, s_{T}^{\prime}) \in \text{Delete}(t) \) if \( s_{T} \) is not allowed to transit to \( s_{T}^{\prime} \); 3) \( (b, s_{T}) \in \text{Relabel}(t) \) if the labeling function of state \( s_{T} \) is updated to \( b \leq 2AP \).

The TS change can be reflected by directly modifying the team automaton using the PA revision strategy in [23]. When a single agent \( r \) receives an update, the latest team automaton is revised by only updating corresponding \( \mathcal{P}(r)(t) \).

Algorithm 2 Local reallocation: environment change

Input: \( \mathcal{P}(r)(t), \text{Path}(r), \text{Info}(t) \)
Output: A new path \( \text{Path}(r)^{+} \)

\[
\text{Path}(r)^{+} \leftarrow \text{empty path} \\
\mathcal{P}(r)(t), \text{R}(t) \leftarrow \text{UpdatePA(\mathcal{P}(r)(t), \text{Info}(t))} \\
\text{if } \text{R}(t) \cap \text{edge(\text{Path}(r))} \neq \emptyset \text{ then} \\
\quad \text{Path}(r)^{+} \leftarrow \text{find-path(\text{Path}(r)(m), \text{Path}(r)(\text{acc}))} \\
\text{else} \\
\quad \text{Path}(r)^{+} \leftarrow \text{Path}(r)(m : ) \\
\text{end if}
\]

Definition 3 (Updating rules). \( \mathcal{G}(t) \) (more specifically, only \( \mathcal{P}(r)(t) \)) is updated given the \( \text{Info}(t) \) from agent \( r \) following the rules:

- If \( (s_{T}, s_{T}^{\prime}) \in \text{Add}(t) \), \( (r, s_{Q}^{\delta}, s_{T}^{\prime}) \) is in \( \delta_{Q}(r, s_{Q}^{\delta}, s_{T}) \) for all \( s_{Q}^{\delta} \) satisfying \( s_{Q}^{\delta} \in \delta_{Q}(s_{Q}^{\delta}, \mathcal{L}(s_{T})) \);
- If \( (s_{T}, s_{T}^{\prime}) \in \text{Delete}(t) \), \( (r, s_{Q}^{\delta}, s_{T}^{\prime}) \) is deleted from \( \delta_{Q}(r, s_{Q}^{\delta}, s_{T}) \) for all \( s_{Q}^{\delta} \in \delta_{Q}(s_{Q}^{\delta}, b) \);
- If \( (b, s_{T}) \in \text{Relabel}(t) \), then \( \forall s_{Q}^{\delta} \in \text{Pred}(s_{T}) \): \( (r, s_{Q}^{\delta}, s_{T}^{\prime}) \) is added to \( \delta_{Q}(r, s_{Q}^{\delta}, s_{T}) \) for all \( s_{Q}^{\delta} \in \delta_{Q}(s_{Q}^{\delta}, b) \); \( (r, s_{Q}^{\delta}, s_{T}^{\prime}) \) is deleted from \( \delta_{Q}(r, s_{Q}^{\delta}, s_{T}) \) for \( \forall s_{Q}^{\delta} \notin \delta_{Q}(s_{Q}^{\delta}, b) \).

If a disturbance was detected on an agent’s TS, a new type of task reallocation algorithm is necessary. Note that no unexpected robot state is assumed in this case and the last matched state is equivalent to the current state, i.e., \( \text{Path}(r)(m) = s_{Q}^{\delta} \). Given the revised local PA \( \mathcal{P}(r)(t) \), we propose a different replanning approach in Algorithm 2, compared to the one in Sec. IV-A.

Proposition 2. In the presence of environmental change and all other agents that are not interfered (i.e., can successfully accomplish their tasks), the global specification \( \phi \) will be fulfilled if a path is found by the local reallocation method in Algorithm 2 on the revised local PA \( \mathcal{P}(r)(t) \).

Proof. According to Algorithm 2, the new state sequence \( \text{Path}(r)^{+} \) starts from the last state \( \text{Path}(r)(m) \) in agent \( r \)'s execution history and reaches the same local accepting state \( \text{Path}(r)(\text{acc}) \). Since the PA updating rules preserve valid NFA transitions, the originally assigned sub-task for agent \( r \) is still fulfilled by the newly found path on \( \mathcal{P}(r)(t) \). Same as Proposition 1, a global action sequence \( \beta \) is formed assuming the rest agents are not interrupted by any disturbances. Consequently, the global specification \( \phi \) is satisfied again.

C. Global reallocation

The two aforementioned local task reallocation approaches do not consider replanning for the whole team, which results in a sub-optimal strategy. Furthermore, if the local task reallocation fails to find a new plan for the agent, a succeeding global task reallocation over the entire team is activated. First, a synchronization step will be executed where the task planner requests for each agent’s current TS state and sets it to be the latest initial TS state \( s_{0,T}^{(r)}(t) \). Then the initial PA set \( S_{0,T}(t) \)
Definition 4 (Synchronized team automaton). The synchronized team model \( R := G(t) \) is an union of N product automata \( P^{(r)}(t) \) given the original product states after synchronization, where \( r \in \{1, \ldots, N\} \) and \( R := (S\text{\textsubscript{R}}, S_{0\text{\textsubscript{R}}}, F\text{\textsubscript{R}}, A\text{\textsubscript{R}}) \) consists of:

- \( S\text{\textsubscript{R}} \) = \{\( (r, s_q, s_T) : r \in \{1, \ldots, N\}, (s_Q, s_T) \in S^{(r)}_P(t) \)\} is the set of states;
- \( S_{0\text{\textsubscript{R}}} \) = \{\( (r, s_Q, s_T) : r = 1, (s_Q, s_T) \in S^{(1)}_0(t) \)\} is the set of initial states;
- \( F\text{\textsubscript{R}} = \{\( (r, s_Q, s_T) \in S\text{\textsubscript{R}} : q \in F \} \) is the set of final accepting states, which remains unchanged since the NFA accepting states are fixed;
- \( A\text{\textsubscript{R}} = \bigcup_r A^{(r)}(t) \cup \zeta(t) \cup \xi(t) \) is the set of actions that include the updated switch transitions \( \zeta(t) \) and the newly proposed synchronized transitions \( \xi(t) \).

Suppose \( \text{ExePath}^{(r)} \) is the executed state sequence acquired from each agent \( r \) and \( \text{ExePath}^{(r)}_Q \) is the projected NFA state sequence. The definition of a synchronized transition is as follows:

Definition 5 (Synchronized transition). The set \( \xi \subset S\text{\textsubscript{R}} \times S\text{\textsubscript{R}} \) denotes synchronized transitions. Each element \( \xi = ((i, s_Q, s_T), (j, s_Q', s_T')) \) satisfies:

- \( i = j \): connects the same agent;
- \( s_Q = \text{ExePath}^{(r)}_Q(\text{init}), s_Q' = \text{ExePath}^{(r)}_Q(\text{final}), r \in \{1, \ldots, N\} \) starts from the initial NFA state and points to the most recent NFA nodes upon request for synchronization of each agent;
- \( s_T = s_T' \): TS state is preserved.

This synchronized transition allows a new transition between two NFA states inside each agent \( P^{(r)}(t) \). Once this is complete, each agent will be aware of the task completion status of the whole team and avoid performing redundant tasks which have already been accomplished. In the original team automaton [29], four properties including correctness, independence, completeness, and ordered sequence are proposed to justify the rationale of finding a global path on the team automaton for a task allocation. Here we claim that our synchronized team automaton preserves those properties, so that a new global action sequence \( \beta \) can be found by applying the same search algorithm performed during the offline phase (as presented in Sec. II). This process leads to a global task reallocation that assigns new sub-tasks to all agents.

Proposition 3. The synchronized team automaton preserves the properties of the original team automaton, i.e., correctness, independence, completeness and ordered sequence.

Proof. The synchronized team automaton distinguishes from the original team automaton in four folds: 1) the set of initial states \( S_{0\text{\textsubscript{R}}} \) is different since the initial PA set \( S^{(1)}_0(t) \) is updated; 2) the set of actions \( A^{(r)}_P(t) \) from each agent \( r \) is updated according to the latest \( P^{(r)}(t) \); 3) the switch transitions \( \zeta(t) \) are removed and then reconstructed after setting current TS state as the latest initial state \( s^{(r)}_0(t) \) for each agent \( r \); 4) the synchronized transitions are added according to the execution history. The first three changes won’t affect the properties of the team automaton in that every state \( s \in S\text{\textsubscript{R}} \) still has an NFA component \( s_Q \) constructed from \( \phi \), and the switch transitions \( \zeta(t) \) are reconstructed under the same definition. As for the fourth change, according to the second condition of Definition 5, new transitions between NFA states are added by connecting the initial and final NFA states from each agent \( r \)’s execution history \( \text{ExePath}^{(r)}_Q \). Although these transitions are not directly provided by \( \phi \), since the states in \( \text{ExePath}^{(r)}_Q \) have already been traversed by agent \( r \), there always exists a sequence of valid NFA transitions between \( \text{ExePath}^{(r)}_Q(\text{init}) \) and \( \text{ExePath}^{(r)}_Q(\text{final}) \). Therefore, synchronized transitions do not change the validness of the original NFA transitions, but only skip the executed transitions. Consequently, all the
properties from original team automaton, including correctness, independence, completeness, and ordered sequence, are preserved.

V. BT Execution Layer

As described in Sec. IV, both local and global task reallocation approaches enable robot recovery from various disturbances and failures. However, certain types of disturbance, such as a loss of balance, require a faster response than others. Therefore, we leverage the reactivity property of BT at the middle level to rapidly select appropriate reactive strategies.

A. Reactive strategies

The decision to execute one reactive strategy over another is determined by the categorized disturbances in Sec. III. Four corresponding types of reactive strategies are specified below.

- **Recovery stand.** This scenario responds to a loss of balance which is specific to legged robots. In this case, the low-level controller on the robot attempts to recover from the fallen state without triggering the high-level LTL planner.

- **Task reallocation: critical failure.** Under this scenario, the robot is deemed incapable of working and therefore, a local task reallocation will be impractical. To resolve this issue, the robot will directly request a global task reallocation assuming a disability to transit to any TS state, to allow the remaining agents to take over its task.

- **Task reallocation: unexpected robot state change.** If this type of disturbance is detected, the planner will locally reallocate its task sequence without the assistance of other robots. If no local plans are feasible, the planner will perform a global task reallocation.

- **Task reallocation: environmental change.** If a robot encounters an environmental change, it will perform a local task reallocation. However, if a solution is not found, a global task reallocation will be performed.

Figure 4. A behavior tree for three levels of reactive strategies is shown. Basic types of BT nodes are thoroughly described in [36]. Yellow oval nodes are condition nodes, and green rectangular nodes are action nodes. R1 is the recovery stand for legged robots, R2 is the reallocation for critical failure, R3 is the reallocation for unexpected robot state change, and R4 is the reallocation for environmental change. Force Failure custom decorator node terminates the BT to execute an appropriate reactive strategy for the specific condition node.

Figure 5. Operating state diagram for legged robot capable of both delivery and training task. Each node refers to robot operating states, whereas each edge refer to an action performed by the robot. Unitree’s A1 quadruped (top left) and UBTECH’s DR (bottom left) are shown as delivery robots, and A1 and UBTECH’s Wassi (top right) are shown as training robots.

B. Behavior tree structure

The BT structure is constructed in the form of precondition → action → effect, which is similar to the works of [26], [35]. This structure allows us to encode all the reactive strategies into separate nodes within a single BT. However, in contrast to their work, we refrain from reconstructing the BT by adding a Repeat decorator node. This enables different robot sensors to check for disturbances at varying frequencies. For example, checking for a “reactive change” would be executed continuously by the Reactive Sequence node, while a “non-reactive change” would only occur prior to receiving a new task. A demonstration of this is shown in Fig. 4 on a quadruped, while the one for a wheeled robot is similar and omitted due to space limit.

VI. Evaluation and Discussion

A. Experiment set-up

To evaluate the feasibility and robustness of the proposed multi-robot task allocation and planning framework, we establish a simulation of a hospital environment in Gazebo [37] and create a topological map for defining the TS, as shown in Fig. 6. The simulation architecture is composed of a high-level LTL planning layer based on a ROS package from [38], a mid-level task execution layer using BehaviorTree.CPP [39], and a low-level navigation and controller layer using ROS navigation stack and appropriate controllers for each robot model. A convex model predictive controller from MIT’s Minicheetah [40], [41] is used to control Unitree’s A1 quadruped over rough terrain, while a conventional holonomic drive model is used on the UBTECH’s DR and Wassi robot. For global path planning, the robot navigates between regions using the A* algorithm [42] and performs collision avoidance with the dynamic window approach [43]. The implementation code is available at https://github.com/GTLIDAR/ltl_multi_agent.

We evaluate our framework on a heterogeneous team of robots consisting of a delivery robot DR, a walk training robot Wassi, and a quadrupedal robot A1 with both capabilities. As shown in Fig. 5, a delivery robot consists of two simple
operating states (Loaded, Standby), where the Standby state is equivalent to Unloaded State. Likewise, a training robot consists of 4 operating states (Standby, Camera On, User Located, Training), where the robot visually locates and helps seniors who need walking training assistance. These operating states are encoded into TS for each type of robots.

B. Case study

We conduct a series of case studies in a hospital environment simulation to evaluate the reactive strategies proposed in Sec. V. The global mission is defined as:

**Scenario.** “Deliver medicines to locations p3 and p6; meet a patient at c1; complete a walk training along the corridor between c1 and c6, and then send the patient back to p4.”

\[ \phi = \Diamond (p3 \land \text{Standby}) \land \Box ((\neg p3 \land \Diamond p3) \rightarrow \text{Loaded}) \]
\[ \land \Diamond (p6 \land \text{Standby}) \land \Box ((\neg p6 \land \Diamond p6) \rightarrow \text{Loaded}) \]
\[ \land \Diamond (p4 \land \text{Standby}) \land \Box ((\neg p4 \land \Diamond p4) \rightarrow \text{Training}) \]
\[ \land \Diamond (c1 \land \text{Training}) \land \Diamond (c7 \land \text{Training}) \land \Diamond (c6 \land \text{Training}) \land \Diamond (c1 \land \text{Training})))]\]

Three robots, A1, DR and Wassi, are placed at various locations in the hospital before the start of the simulation. Next, the task planner decomposes the specification and assigns sub-tasks to each robot offline. During the simulation, each robot will encounter a disturbance. A diagram of this simulation is displayed in Fig. 6. More details can be found in the video3.

1) External force is applied to A1 and induces a loss of balance. A handcrafted whole-body recovery stand trajectory is tracked by a PD controller to assist A1 to resume its task.

2) A critical failure is induced for Wassi when performing the walk training task from c7 to c6. A global reallocation strategy assigns A1 to complete its delivery task first, and then proceeds to finish Wassi’s incomplete walk training task.

3) The Loaded state of DR suddenly becomes a Standby state. This simulates a situation in which the robot unexpectedly loses its cargo. A local reallocation succeeds in instructing the robot to return to s1 and pick up another cargo. Then DR is instructed to complete the original delivery task.

4) A garbage pile is placed in front of p3 to simulate an environmental change. This obstruction can only be traversed by the legged robot A1. The routes taken by each robot and the timeline for obstacle detection and task allocation are portrayed in Fig. 6. While performing its task, DR encounters the obstruction and fails to find an alternate plan via local reallocation. While A1 is returning home after completing the delivery task to p6, it is assigned to take over DR’s incomplete delivery task at c4. As a result, A1 goes to s1 to retrieve the object for delivery, and completes the task by traveling to p3.

In addition to applying individual disturbances, we also evaluate the same scenario ten times with random adversarial environment inputs. In each case, pedestrian models are generated in the simulation to follow different navigation paths within the environment. Furthermore, the initial configuration for each robot is modified to prompt a different offline allocation result. During the runtime simulation, signals indicating robot state and environmental changes are randomly sent to each robot and prompt their reactive behaviors. As shown in Table I, we report the times at which the reactivity strategy is triggered and the average computation time it takes for ten trials. Our framework demonstrates 80% successful rate of completing the global mission \( \phi \). Mission-level failures occur when more than one robot undergoes a critical failure, which causes the remaining task to be unachievable. A global task reallocation could result in a more optimal task sequence in principle but require a synchronization step for all agents and expensive computation.

### Table I

|                  | R1 | R2 | R3 | R4 |
|------------------|----|----|----|----|
| Triggered times  | 18 | 16 | 10 | 16 |
| Local reallocation time (s) | -  | -  | 0.023 | 0.018 |
| Global reallocation time (s)   | -  | 3.31 | 2.95  | 3.42 |

VII. Conclusion

In this work, we present a heterogeneous, multi-robot task allocation and planning framework equipped with a hierarchically reactive mechanism from extensive disturbances. A local
and global task reallocation is performed at the high level where an LTL-based team automaton is generated to follow a formal guarantee. At the middle level, a BT framework is incorporated to promptly select different replanning strategies which can be executed at different rates. Lastly, all the work mentioned is showcased in a dynamic simulation of a hospital environment involving quadrupeds and wheeled robots.

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