

VVUQ of a thermal-hydraulic multi-scale tool on unprotected loss of flow accident in SFR reactor

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Abstract. Within the framework of the French 4th-generation Sodium-cooled Fast Reactor safety assessment, methodology on VVUQ (Verification, Validation, Uncertainty Quantification) is conducted to demonstrate that the CEA’s thermal-hydraulic Scientific Computation Tools (SCTs) are effective and operational for design and safety studies purposes on this type of reactor. This VVUQ-based qualification is a regulatory requirement from the French Nuclear Safety Authority (NSA). In this paper, the current practice of VVUQ approach application for a SFR accidental transient is described with regard to the NSA requirements. It constitutes the first practical, progressively improvable approach. As the SCT is qualified for a given version on a given scenario, the transient related to a total unprotected station blackout has been selected. As it is a very complex multi-scale transient, the SCT MATHYS (which is a coupling of the CATHARE2 tool at system scale, TrioMC tool at component scale and TrioCFD tool at local scale) is used. This paper presents the preliminary VVUQ application to the qualification of this tool on this selected transient. In addition, this work underlines some feedback on design and R&D aspects that should be addressed in the future to improve the SCT.

1 Introduction

In the framework of the French 4th-generation Sodium-cooled Fast Reactor (SFR), numerical simulations are performed to assess the design and the safety features of the nuclear facility. These simulations are realised with Scientific Calculation Tools (SCTs) that must be beforehand qualified according to the VVUQ (Verification, Validation, Uncertainty Quantification) approach. This VVUQ-based qualification is a regulatory requirement from the French Nuclear Safety Authority (NSA) formalized in the guide number 28 of NSA released in July 2017 [1]. This qualification guarantees the availability of effective and operational SCT for design and safety studies purposes. These tools enable to limit the conservatisms and thus to reduce the margins and sources of extra-costs (component design, prevention devices, etc...). The ultimate goal of VVUQ activities is to assist decision makers intaking aware decisions about an intended application.

While the NSA requirements are increasingly considered to qualify scientific tools used in the safety demonstration of Pressurized Water Reactors (PWR), the applications of the VVUQ methodology for some PWR transients, such as the Loss-Of-Coolant Accident (LOCA), have raised the difficulty of a strict application of these requirements. For example, EDF and Framatome have developed for this application a Best Estimate Plus Uncertainties (BEPU) methodology named CathSBI (Cathare Statistical Intermediate Break) which is designed to study Intermediate Break (IB) LOCA [2]. The CathSBI methodology, in addition to the consideration of multi-physics (fuel related) phenomena, includes some new features, notably the use of 3D thermal hydraulic modules of the CATHARE code. This is a first use in France in safety analyses and raised several issues [3]; indeed the methodologies usually involve only 0D-1D flow simulations. Moreover in this framework of PWR safety demonstration, a lot of work is still ongoing on simulation tool validation and quantification of TH code model input uncertainties. The validation is an on-going process taking advantage of the always new experimental facility results. The input uncertainty quantification (IUQ) on the physical models still requires further investigations, even if this issue has already been tackled in the past through three OECD/NEA projects: Best-Estimate Methods Uncertainty and...
Sensitivity Evaluation (BEMUSE) [4], Post-BEMUSE Reflood Models Input Uncertainty Methods (PREMIUM) benchmark [5], Systematic APproach for Input Uncertainty quantification Methodology (SAPIUM). Indeed, the analysis of PREMIUM phases III and IV benchmark results has shown a large dispersion results between participants [6]. One main reason could be attributed to the lack of common consensus and practices in the followed IUQ process and method. Thus in France, even in the PWR safety demonstration, the establishment of the tool quantification (VVUQ) methodology, which should in addition be adapted to each safety transient, is not terminated.

There is not recent published VVUQ application on SFR transients in France. In fact, since the SuperPhénoix reactor, the SFR safety demonstration has not been addressed in France. Furthermore, this demonstration should nowadays follow the regulatory requirements from the French NSA, which is a novelty compared to the SuperPhénoix safety demonstration. In Japan, lots of studied have been carried out on the prototype SFR MONJU, the Japanese experimental SFR JOYO and finally the Japan Sodium-cooled Fast Reactor (JSFR). For the commercialization of SFRs in Japan, V&V procedures have been developed and, on some specific transients, statistical evaluations of the main safety variable (core hot spot temperature) have been performed [7]. Nonetheless, VVUQ method is not systematically followed for safety demonstration in Japan. Much effort has been devoted to the establishment of the “Safety Design Criteria (SDC)” for the Sodium-cooled Fast Reactor (SFR) system [8]. The objective of the SDC is to provide a set of general criteria for the safety designs of structures, systems and components of the Generation-IV Sodium-cooled Fast Reactors (Gen-IV SFRs), where the criteria are clarified systematically and comprehensively, and are consistent with the GIF’s basic safety approach and with the aim of achieving the safety and reliability goals defined in the GIF Roadmap [9]. These SDC have been disseminated, updated and utilized for SFR designing worldwide. For these activities, harmonious interaction has already been started among research and design organizations of SFRs, regulatory bodies and their technical support organizations and international organizations such as IAEA and OECD/NEA [10]. Among the TH issues related to SDC, there notably are the natural circulation decay heat removal and the highest temperature evaluation in a subassembly of the core [11]. Indeed, liquid sodium has high thermal conductivity and high boiling temperature at atmospheric pressure, allowing to consider in the safety approach the remove of decay heat by the natural circulation of the coolant as a passive safety system. As an SFR is operated under low pressure conditions, coolant leakage does not lead to the type of loss of coolant accident anticipated in a PWR involving depressurization, coolant boiling and the loss of cooling capability. Therefore, unlike a PWR, emergency core cooling systems for coolant injection under high and low pressure conditions are not necessary for an SFR. The only requirement for SFR core cooling is the retention of the sodium coolant level above the reactor core in the reactor vessel along with sufficient heat removal capability and that the maximum clad temperature does not exceed the saturation temperature.

This paper addresses these issues related to SFRs Safety Design Criteria through the application of the VVUQ methodology for Scientific Computation Tool simulating a complex 3D TH transients in the French SFR prototype with regard to the French NSA requirements. It constitutes the first practical, progressively improvable approach on VVUQ application on a SFR transient. As the SCT is qualified for a given version on a given scenario, 19 transients have been identified for SFR safety demonstration from a Phenomena identification and Ranking table evaluation (PIRT) [12]. Among them, the transient related to a total unprotected station blackout has been selected [13] (Sect. 2.2). This is a 2 h-time frame scenario which belongs to the Operating Situation of category 4 safety scale. Indeed this transient is one of the most 3D complex, involving thermal stratification in the upper and lower plena, natural circulation inside the main vessel and the primary loops. Moreover as the SDC is a local sub-assembly variable (the local maximum clad temperature), the simulation of this transient thus requires a multi-scale coupling of several thermal-hydraulic SCT to correctly capture the main 3D phenomena and the safety output results, taking into account all the associated uncertainties.

But as, it is not practicable to simulate the whole reactor in 3D, the SCT MATHYS (Multi-scale ASTRID Thermal-hydraulics) which features a coupling of CATHARE2 at system scale, TrioMC at component scale and TrioCFD at local scale is therefore required for this study.

After a slight description of the French SFR reactor in Section 2, this paper will present the VVUQ application to the qualification of the MATHYS SCT on this unprotected total station blackout transient in Section 3. It breaks down the steps of verification, validation (which confronts the domain of applicability/utilization to its domain of validation) and the quantification of various sources of uncertainties (boundary conditions, input, scenario, model...). In addition, this work presents the propagation and post-processing of a high number of parameters in Section 4. These results also leads to a first feedback on this reactor design. Some R&D aspects will also be addressed.

2 The SFR project

In the framework of the French SFR construction project, numerical simulations are performed to assess the design and safety of the reactor.

2.1 French SFR reactor

The studied French SFR reactor [14] is a pool type reactor composed of a main primary circuit, four sodium secondary loops and a power conversion system. It gathers some evolutions from the past reactors (SuperPhénoix…) enabling to increase it safety level to the GEN IV reactors
requirements. Focusing on the core, the majors improvement is the CFV core (low sodium void effect core). This new core concept is an axial heterogeneous core of 1500 MWth on the contrary to more classical homogeneous cores used in former SFR. The low sodium void effect of the CFV core results mainly from the presence of a sodium plenum above the fissile zones combined to the presence of a fertile plate in the inner zone of the core encompassed by two fissile zones (displayed in Fig. 1). The larger height of the outer fissile zone enables the void reactivity effect to be lowered as well, due to neutron leakage enhancement [15]. Other innovative features of this reactor concern the core-catcher, the system of energy conversion, the inspectability of the in-core components, passive decay heat removal systems (Direct Heat Removal – DHR). These systems, though responsible for major safety improvements, tends to induce new, hard-to-model physical phenomena. For instance, DHR systems at the top of a pool-type SFR tend to cool the core via several competing natural convection paths inside the core [16].

Figure 2 shows the schematic of this SFR primary circuit. The main vessel is around 18.5 m high and 16 m in diameter. It contains several passive and active decay heat removal systems. The nominal primary flow rate is around 8500 kg/s from which 7900 kg/s goes through the core. The latter is composed of an inner core, an outer core, neutron-shielding and internal fuel storage [17,18]. Passive complementary safety devices such as hydraulically suspended absorber rod sub-assemblies (called RBH) are also part of the design [19].

### 2.2 Studied transient

The VVUQ process is applied to a calculation tool dedicated to the simulation of one reactor in one operating situation for design, safety analysis and operation. Its final objective is to give the proof of the tool adequacy for this application with the quantification of the whole set of uncertainties. As the scientific tool is qualified for a given
version on a given scenario, 19 transients have been identified for this SFR safety demonstration. These main types of transients are issued from many years of studies on SFR, especially on Phenix, Superphenix and EFR [20] and PIRTs on TH issues on SFR [12]. By the way, this has led to a development plans of multiphysics [21] or multiscale simulations [16] tools. The originality of this paper resides in the selection of 19 incidental or accidental transients, belonging to five families of transients (reactivity variations, defect of primary circuit cooling, defect of sub-assembly cooling, defect of secondary and tertiary circuits cooling, loss of function supporting) and their associated classification in the situation categories given in a Framer’s diagram (composed of four types of Operating Situations (OS), Prevention Situations (PS), Mitigation Situations (MS) and Practically Eliminated Situations). This classification aims at identifying the safety output variables for each transient. The adapted simulation tool for each simulation has been identified focusing on the main phenomena driving each transient and thus the required scales of resolution of TH in the various part of the reactor. These transients are reported in Table 1 with the scientific tools required for their simulation and the associated safety output variables to the various situation categories are given in Table 2.

As the aim of this work is the demonstration of the feasibility of the VVUQ methodology and its first application on SFR scope, only one transient among the 19 identified transients (Tab. 1), the Unprotected Station BlackOut shorter than 2h (USBO) [13], has been selected for demonstration purpose of the practical applicability of this VVUQ methodology with regard to the NSA

**Table 1.** 19 transients selected for this SFR safety demonstration (SA: Severe Accident).

| Family                              | Description                                                                 | Situation category | Scientific calculation tool |
|-------------------------------------|-----------------------------------------------------------------------------|--------------------|-----------------------------|
| Loss of function supporting         | General slowdown of the primary pumps                                       | OS2                | CATHARE2                    |
|                                     | General acceleration of the primary pumps                                    | OS2                | CATHARE2                    |
|                                     | Seizure or shaft failure of one primary pump                                 | OS3                | MATHYS                      |
|                                     | Connection failure between a primary pump and diagrid                         | OS4                | MATHYS                      |
|                                     | Unprotected general slowdown of the primary pumps                             | PS                 | MATHYS                      |
|                                    | Partial blockage of a fissile sub-assembly                                   | OS3                | MATHYS                      |
|                                    | Partial blockage of an absorbent sub-assembly                                | OS3                | MATHYS                      |
|                                    | Progressive melting of a sub-assembly owing to a blockage                    | PS                 | SIMMER (SA)                 |
|                                    | One or several secondary pump trips                                          | OS2                | CATHARE2                    |
|                                    | Unintentional draining of secondary loops                                    | OS3                | CATHARE2                    |
|                                    | Unintentional closure of isolation valve on secondary loops                  | OS4                | CATHARE2                    |
|                                    | Station BlackOut shorter than 2 h                                            | OS2                | CATHARE2                    |
|                                    | Station BlackOut longer than 2 h                                             | OS3                | CATHARE2                    |
|                                    | Generalized under-voltage shorter than 3 days                                | OS4                | MATHYS                      |
|                                    | Unprotected Station BlackOut shorter than 2 h                                | OS4                | MATHYS                      |
|                                    | Unintentional rising of a control rod                                        | OS2                | Multiphysic Tool            |
|                                    | Unintentional drop of a control rod                                          | OS2                | Multiphysic Tool            |
|                                    | Unintentional automatic reactor shut-down                                    | OS2                | MATHYS                      |
|                                    | Unintentional fast reactor shut-down                                         | OS2                | MATHYS                      |

**Table 2.** Decoupling criteria resulting from general safety criteria.

| Category | Decoupling criteria on cladding                                      |
|----------|---------------------------------------------------------------------|
| OS1      | MCT < 700 °C                                                        |
| OS2      | 700 °C < MCT < 750 °C less than 10’s                                |
|          | 750 °C < MCT < 800 °C less than 3’                                   |
|          | MCT > 800 °C forbidden                                               |
| OS3      | Same as OS2                                                         |
| OS4      | MNaT < T Sat                                                        |
|          | MCT < 800 °C                                                        |
| PS       | MNaT < T Sat                                                        |
|          | MCT < 825 °C                                                        |
|          | Tmax hexagonal wrapper < 800 °C                                     |
| MS       | Mechanical Energy < [100 ;300] MJ                                    |

MCT, Maximum Clad Temperature; MNaT, Maximum Sodium Temperature.
requirements. This is a 2 h-timeframe scenario which belongs to an Operating Situation of Category 4 safety scale. Indeed this transient is one of the most complex single physic transient (thermal-hydraulic physics), involving thermal stratification in the plena and natural circulation inside the main vessel and the primary loops. It thus requires the multi-scale coupling of the MATHYS tool to correctly capture the main safety output results (the local maximum clad temperature and the sodium temperature at the outlet of the core – Tab. 2).

During this USBO accident, the following events of this USBO accident are given in Table 3.

At \( t = 0 \) s, the scram signal is sent, the Primary Pumps (PP) trip and the shutdown of secondary (EMP) occur. The primary and secondary flow rates decrease leading to the increase of the core temperature. As the primary flow rate decreases, it reaches a design threshold (45\% of nominal flow rate) which leads to the drop of the hydraulic prevention control rods (RBH). These rods are fully inserted in the core in 3 s. As they insert 722 pcm antireactivity per rod, after this 3 s delay only residual power needs to be removed. Other prevention control rods are designed on this reactor: the magnetic control rods (RBD) which fall when the sodium temperature at the outlet of the core exceeds 650 °C. When the flow rate is low and sodium thermal stratification is established, natural circulation in the primary circuit then occurs due to buoyancy effects (sodium being heated in the core and cooled in the Intermediate Heat Exchangers (IHX)). Natural circulation in the secondary circuit increases the heat removal during the first 1000 s. After \( t = 1000 \) s, primary heat is no longer removed by the IHX. Residual power is nonetheless removed from the core thanks to the flow through the inter-wrapper (gap between hexagonal tubes surrounding the sub-assemblies). While the flow pattern changes in the Hot/Cold pools (large volumes above and below the core), the temperature slowly rises.

The Complete Computational Fluid Dynamics (CFD) domain nearly covers all the vessel (Fig. 3). Indeed, this transient involves 3D flow patterns in the pools, in the inter-wrapper gap and the primary side of the IHX. In addition, stratification of the sodium has a huge impact on the inlet temperatures of the PP and IHX, which, during the transient, impact greatly the natural circulation (Fig. 4). This is why local simulation involving CFD calculations are required to properly account for these phenomena. Because of the high cost in time of CFD computations and the need to take into account external models such as neutronics (point kinetics in MATHYS) or PP performance maps, TH multi-scale and TH-neutronic multi-physics coupled solutions are applied to perform the calculations. In particular, the onset of natural circulation needs to be evaluated, along with sodium and cladding temperatures in the core (which are the outlet variables of interest). Furthermore, using multi-scale thermal-hydraulics coupled calculation tools enables to describe as precisely as possible the major structures (Above CoreStructure (ACS), Hot and Cold Plenum (HP and CP), sub-assembly and inter-wrapper gap for instance) and physical phenomena (buoyancy driven flow and inter-wrapper reversal flow for instance) while still maintaining a reasonable computing time effort. These computations involve advanced coupling methodologies. More details on this multi-scale model used for the coupled calculation can be found in [13]. The left side of Figure 4 illustrates the primary circuit temperature field under nominal conditions, calculated by MATHYS whereas the right side shows the benefit of a multiscale TH simulation of this transient which enables to obtain the main phenomena identified by the PIRT [12].

- the pool stratification and heat transfer between pools which affect natural convection in the complete primary circuit;
- the inter-wrapper flow heat removal (and more generally of radial heat transfers in the core) and its effects on the hot pool thermal-hydraulics, as well as sodium recirculation in the core. The plena stratification is in turn influenced by the behavior of the sodium jets coming out of the core into the hot pool, and out of the IHXes into the cold pool; these jets are velocity-driven in forced convection, but turn upwards under the effect of buoyancy in natural convection.

### Table 3. USBO events timeline.

| Time       | Events                                                                 |
|------------|------------------------------------------------------------------------|
| \( t = 0 \) s | Trip of Primary Pumps (PP) Stop of secondary Electromagnetic Pump (EMP) |
| \( t = 1000 \) s | Secondary circuit insulation (primary to secondary circuit thermal exchanges are observed to be null) |

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3 VVUQ application

In France, a professional guide was published in 2019 for PWR giving the main orientations to be followed by industrials (designers and operators of nuclear plants) to answer optimally to the recommendations of guide number 28 of NSA issued in July 2017 [1]. This guide states that, for a given transient, a SCT can be regarded as qualified when the VVUQ assessment (including scaling related uncertainties) has been properly completed. Concerning the qualification of a chaining or coupling of several tools (here, various thermal-hydraulic tools), the guide specifies that “there should not in principle be any difference in terms of qualification requirements by comparison with the case of a single tool”. Consequently a VVUQ process was then achieved for the coupled multi-scale tool MATHYS version v1.7.3. The qualification, which demonstrates the MATHYS adequacy for the realistic simulation of a USBO transient, has to provide the quantification of the whole set of uncertainties associated with the calculation of this situation or scenario.

Once the tool qualification is achieved, operators of nuclear plants could use this tool for safety demonstration. Based on these tool simulationsthey verify that the reactor is kept in a state which fulfilled the safety requirements (concerning the control of neutron reaction chain, decay heat removal and thus coolability of the reactor). For this purpose, it is necessary to demonstrate that the safety criteria representing the phenomenon of interest are verified with a certain margin. The safety margins provide an over-dimensioning which enables to overcome situations that would not be taken into account in the design. These safety criteria dictate the studied output variables (or Figures of merit) in the safety demonstration. These variables depend on the transient category. Here, for USBO accident which lies in the Operating Situation of category 4 on the safety scale, the criteria are the following (Tab. 2):

- the temperature of the sodium should remain below the saturation temperature;
- the maximum clad temperature should remain, taking into account the uncertainties, below 800°C.

These quantified decoupling criteria reflect a qualitative general safety criterion which stipulates that general clad fusion should not occur but some local fusion could be tolerated if their consequences remain limited.

The objective of this preliminary demonstration is to obtain the mentioned figures of merit and associated uncertainties for an USBO scenario by means of applying the MATHYS SCT; therefore, fulfilling each VVUQ step in the process.

3.1 Verification step

This step, which aims demonstrating that the equations are correctly solved from the numerical and data processing point of view, is accomplished for each tool (CATHARE2, TrioMC and TrioCFD) coupled inside MATHYS and is reported in the release notes of each tool and version specifying the used. This verification step is done as it is commonly the case. Equations in the simulations tools are checked: mass, energy and momentum are correctly solved and data transfer between components in the MATHYS tool are properly done. Moreover, as several situations are studied for the safety demonstration, the difficulty is to have a unique type of TH tool coupling for the simulation of each multiscale simulation. This was solved, at CEA, through the development of the unified “coupling tool”, called MATHYS, as a way to ensure that the same coupling algorithm is being applied in all cases. In this way, the verification step is reinforced. In MATHYS, the links and the interfaces between tools have also been verified. The coupled platforms developed in CEA (and MATHYS...
among them) solve the interface between codes using an API called ICoCo [22]. This code enables function calls for every coupled code such as information transmission, time step iteration or process.store/retrieve operations. The order in which the functions are called is based on the coupling methodology explained in details in [13]; TrioCFD and TrioMC are coupled using the domain decomposition method whereas the coupling between CATHARE2 and TrioCFD-TrioMC uses the domain overlapping method [13].

3.2 Validation step

This step commonly relies on the numerical validation by comparison with reference tools and/or analytical solutions, and on experimental validation by comparison with experimental data. More recently, efforts have been made to support these multi-scale approach with a comprehensive validation database relying, as for TH codes at various scale, on experiments at the separate-effects, combined-effect and integral scales. This experimental database consists of:

– Separate Effect Tests (SETs) dedicated to the study of each physical phenomenon relevant to the final reactor application in representative conditions;
– Integral Effect Tests (IETs), capable of reproducing interactions between these phenomena that may occur in the final reactor case;
– System and Integral Tests (SITs), or reactor-scale integral tests where all phenomena may come into play.

This validation work is properly documented [13,23,24]. The complexity of this validation arises from considering the case of a coupling between three existing codes, such as a system/sub-assembly/CFD codes coupling, where each of the codes usually benefits from an existing validation database. Counter-intuitively, this individual validation is not sufficient to validate the coupled tool itself, as the introduction of interactions between scales may lead to new physical phenomena, or new interactions, which are not covered by the codes’ individual validation matrices. For USBO transient, this interactions lead to, as already explained:

– pool stratification and heat transfer between pools on natural convection in the complete primary circuit;
– inter-wrapper flow heat removal (and more generally of radial heat transfers in the core) on hot pool thermal-hydraulics and on overall natural convection.

Constructing a validation matrix for the multi-scale tool then requires identifying separate-effects, integral effects and integral tests suitable for validating these phenomena and their interactions during the considered USBO transient.

However, it is important to underline that the experimental database for the validation of tools dedicated to SFR is far smaller than the one dedicated to PWR. Moreover, validating main TH phenomena at the system scale would require a high level of geometrical similarity, and thus adapted experiments for the studied new design. In contrast, the ability of CFD to simulate geometrical effects directly makes it easier to argue that experiments performed for other designs (and thus in different geometrical configurations) will provide a useful contribution for validating the new tool. Thanks to these arguments, multi-scale/CFD tool may thus rely on a growing experimental database for validating coupled effects:

– for the effect of pool thermal-hydraulics on natural convection, TALL-3D [25] (SET), CIRCE-HERO [26] (IET) and E-SCAPE [27] (IET) may be considered;
– for the effect of inter-wrapper flow on S/A cooling, THEADES [28] (SET), PLANDTL-1 [29] (IET) and PLANDTL-2 [30] (IET) are available or will be in the near future;
– CLEAR-S [31] (IET) will present an interesting case where it will be possible to validate the effect of pool TH and inter-wrapper flow on global natural convection at the same time;
– for integral validation, PHENIX [24], EBR-II [32] and FFTF [33] tests are or will be available in the short-term.

These tests span two reactor types (loop for PLANDTL1/2 and FFTF, pool for all others) and two working fluids (sodium or Lead-bismuth eutectic) as well as several design types: nevertheless, thanks to the geometrical genericity of multi-scale/CFD tools, they may all contribute to validating the application of the MATHYS tool on the studied USBO domain of utilization.

This domain of utilization of the MATHYS tool has been characterized by occurrence of main phenomena and expressed in ranges of pressure, core flow rate (and thus velocity), temperatures and dimensionless numbers such as Reynolds number. These variables feature the reactor conditions along this transient. To define this scope using a selected influential parameters turns out to be a laborious exercise as the variables change with time. The domain of utilization can hardly be defined in detail, hence a macroscopic approach prevails. According to the VVUQ methodology, this domain of utilization should be compared to the domain of validation of MATHYS, that is, the respective domains of validation of CATHARE2, TrioMC and TrioCFD corresponding to their domains of use in the reactor; for example the whole loop for CATHARE2, the two plenums, the ACS and the inter-wapper zone for TrioCFD, and the core sub-assemblies for TrioMC. Whereas the domains of validation of TrioMC and TrioCFD are quite well restricted, this is not the case for CATHARE2. As a result of the generalist nature of the CATHARE2 tool, experiments upon which are based its validation cover wide ranges of physical variables. The direct consequence is that the validation domain is also defined in a very macroscopic manner in the CATHARE2 validation reports. Furthermore, as it is difficult to cover, with the validation domain the domain of utilization, it might be somehow demonstrated (by sensitivity studies for example), that a lack in the validation domain might not have an influence on results of interest.

From this preliminary attempt to rigorously draw and compare the domain of utilization and the domain of validation on this complex USBO transient, it is concluded that the establishment of a precise methodology to achieve
The uncertainties are of diverse natures: input or scenario uncertainties, linked to the reactor design options are given in Table 4 from design reports with their associated probabilistic distributions. There are of course constraints which link the elements of the core geometry together in order to respect volume conservation. This will be taken into account through a constrained Monte Carlo experimental design (Sect. 4). Moreover, as the Best Practices Guidelines are meticulously followed for the 3 tools, the numerical bias are considered negligible. The scaling/transposition uncertainties are not taken into account as discussed in the above section because the methodology to estimate them is not mature. The main scenario uncertainties have been selected through expert judgment of realistic transients, or bibliographic databases on past SFRs or sensitivity studies (see Tab. 5). Among them, we can notice the power level at the transient beginning, the main USBO transient feature; flow rate drop trigger value for the RBH rods is also important. The RBD rods are not considered in this list because, after several sensitivity studies, it happens that never reaches the RBD triggering threshold during such transients.

The final work in this section aims at quantifying the influential uncertainties associated with the physical MATHYS tool models. As already explained, determining the input uncertainty quantification on the physical models still requires further investigations in PWR framework where a far larger amount of experimental data than for SFR is available. In PWR scope, these uncertainties are deduced from the validation step by the CIRCE (Inverse Quantification of Uncertainty) method [35] developed by CEA. This method has been extensively applied to the

### Table 4. Design uncertain variables linked to the core geometry—truncated normal law at ±3σ.

| Design variables                  | Nominal value (at 480°C) | Derivation (σ) | Inf limit (−3σ) | Sup limit (3σ) |
|-----------------------------------|--------------------------|----------------|-----------------|---------------|
| Pin diameter (mm)                 | 9.790                    | 0.075          | 9.736           | 10.015        |
| Clad thickness (mm)               | 0.5042                   | 0.0199         | 0.4445          | 0.5639        |
| Spacer wires diameter (mm)        | 1.0084                   | 0.0200         | 0.9884          | 1.0684        |
| Internal distance between flats (mm) | 162.460                | 0.305          | 161.545         | 163.375       |

Table 5. Main scenario uncertainties — truncated normal law at ±3σ.

| Scenario variables                          | Uncertainty range at (±2σ) | Nominal value | Derivation (σ) | Inf limit (−3σ) | Sup limit (3σ) |
|---------------------------------------------|----------------------------|---------------|----------------|-----------------|---------------|
| Initial reactor power                       | ±5%                        | 1500 MW       | 2.5            | −7.5            | 7.5           |
| Residual power                              | ±20%                       | Calculated decrease (neutronic results) | 10             | −30             | 30            |
| Primary pumps inertia                       | ±20%                       | 8000 kg.m²    | 10             | −30             | 30            |
| % of primary flow rate; criterion for RBH rods triggering | ±20%                     | 45%           | 10             | −30             | 30            |
| Anti-reactivity of one RBH rod              | ±5%                        | 722 pcm       | 2.5            | −7.5            | 7.5           |
| Fall duration of RBH rods fall              | ±20%                       | 3 s           | 10             | −30             | 30            |

this comparison is necessary; not to miss an important part of the validation domain. Moreover, at this stage, it is obvious that the domain of utilization for USBO cannot be encompassed within the domain of validation of MATHYS because some validation part of works are done on scaled experiments, possibly using simulating fluids. Thus, even if the general phenomenon of interest is reproduced during this experiment, the ranges of influential variables do not correspond to the one of the domain of utilization. A transposition of this validation work should then be realized to the domain of utilization. By doing this, the domain of validation of the MATHYS tool becomes its domain of validity. This consists in the transposition or scaling step, sometimes added to the VVUQ. This step is dedicated to the extrapolation of the validation results to the intended scope of utilization considering the scale effect and the possible physical differences. Nowadays, and although some studies have been performed in this sense [34], the methodology to achieve this scaling or transposition step is still fledging and much belongs to R&D activities. It is commonly conceded that this step might lead to the quantification of particular uncertainties, linked to the move of the domain of validation to the domain of validity, called transposition uncertainties. In this present work, which consists on a preliminary application of the VVUQ methodology in SFR scope, these uncertainties have not been determined and less neither propagated.

### 3.3 Uncertainty quantification step

The uncertainties are of diverse natures: input or scenario uncertainties, design uncertainties, model uncertainties, numerical bias (temporal/spatial uncertainties), scaling/transposition uncertainties. In this study, the uncertainties linked to the reactor design options are given in Table 4 from design reports with their associated probabilistic distributions. There are of course constraints which link the elements of the core geometry together in order to respect volume conservation. This will be taken into account through a constrained Monte Carlo experimental design (Sect. 4). Moreover, as the Best Practices Guidelines are meticulously followed for the 3 tools, the numerical bias are considered negligible. The scaling/transposition uncertainties are not taken into account as discussed in the above section because the methodology to estimate them is not mature. The main scenario uncertainties have been selected through expert judgment of realistic transients, or bibliographic databases on past SFRs or sensitivity studies (see Tab. 5). Among them, we can notice the power level at the transient beginning, the main USBO transient feature; flow rate drop trigger value for the RBH rods is also important. The RBD rods are not considered in this list because, after several sensitivity studies, it happens that the sodium temperature at the top of the sub-assemblies never reaches the RBD triggering threshold during such transients.
Table 6. Main model parameters uncertainties (1/2) – truncated normal law at ±3σ (neutronic best estimate data issued from the ERANOS tool [37] and thermo mechanical (TM) data issued from GERMINAL [38]).

| Modeled variable                                                   | Uncertainty range at ±2σ | Nominal value | Derivation (σ) | Inf limit (−3σ) | Sup limit (+3σ) |
|-------------------------------------------------------------------|--------------------------|---------------|----------------|-----------------|-----------------|
| Neutronic feedback due to fuel axial thermal expansion             | ±25%                     | List of neutronic data* | 12.5           | −37.5           | 37.5            |
| Doppler neutronic feedback                                        | ±15%                     | List of neutronic data* | 7.5            | −22.5           | 22.5            |
| Sodium void/density neutronic feedback                            | ±20%                     | List of neutronic data* | 10             | −30             | 30              |
| Pellet/clad heat transfer coefficient                              | ±20%                     | List of TM data*      | 10             | −30             | 30              |
| Clad conductivity                                                 | ±5%                      | 19.52 (W/m/°C)      | 0.50           | 18.02           | 21.02           |
| Singular head loss at the bottom of each sub-assembly             | ±10%                     | Depending on flow rate | 5              | −15             | 15              |
| Singular head loss at the bottom of storage sub-assembly          | ±10%                     | 8648            | 5              | −15             | 15              |
| Singular head loss at the bottom of sub-assembly in debugging positions | ±10%                    | 3095            | 5              | −15             | 15              |

*For some data (neutronic or TM), one particular value is defined for one group of sub-assemblies and/or for one axial mesh.

Thus, in this preliminary study, uncertainties on data of others physics are derived from sensitivity studies and uncertainty propagations with others SCT like ERANOS [37] (for the neutronics) and GERMINAL [38] for thermo mechanics.

Finally, the models uncertainties propagated through MATHYS in the USBO transient are reported in Tables 6 and 7, with their associated probabilistic distributions. These lists have been restricted to the main influential model parameters determined beforehand from sensitivity studies and the uncertainties are issued from literature review [39–41].

In the end, 23 uncertain variables have been quantified. This step also includes the determination of the appropriated method for the uncertainties propagation through the simulation. The USBO transient belonging to the Operating Situation of Category 4 safety scale, a BEPU method is recommended for the realization of uncertainties propagation, contrary to a penalized Realistic Deterministic method recommended in case of transients belonging to operating conditions categories 1–3.

At this stage, all the steps of the VVUQ methodology for the qualification of the MATHYS tool on a USBO transient are fulfilled. The propagation of the uncertainties, presented in the next section, is done for assessment purpose. Furthermore, it might be interesting to investigate if the results of propagation and the associated Global Sensitivity Analysis (GSA) depend on the PDF ‘Probability Distribution Function’ assumptions concerning the uncertain variables. In the framework of sensitivity analysis, authors [42] has recently proposed a solution to...
evaluate the impact of uncertainty on input distributions that they referred as “second-level uncertainties”. This will be examined in the future.

4 Uncertainties propagation results

To propagate the 23 uncertain input variables presented in the previous section, a constrained Monte Carlo experiment (of the uncertain inputs) is built. It consists in generating a greater number of Monte Carlo draws according to the marginal laws of the input variables, independently (i.e. without constraints), and then only keeping the simulations which respect the constraints. This technics leads to a Monte Carlo sample of independent and identically distributed according to the joint distribution of the inputs. From this coarse process, it is derived 136 simulations of USBO transient corresponding to realistic scenario. Each simulation is very CPU consuming and required a High Performance Cluster (HPC); each simulation requires 308 processors and a CPU time of 3 days for around 4000 s of transient.

Because of this very high CPU time, the number of studied simulations results from a compromise between the CPU time required for each simulation and the number of input parameters. Even if the considered sample is smaller than the rules of thumb issued from literature [43] (which propose a sample at least as large as 10 times the dimension of the input vector), it was considered as optimal because the obtained Gaussian process metamodel1, built to model and predict the first temperature peak, exhibits a high and very satisfactory predictivity of $Q^2 = 0.99$ (99% of the variance of the first temperature peak is explained by the surrogate model). Indeed, to circumvent the issue of our CPU expensive simulator, a widely accepted method consists in replacing the CPU-time expensive computer models by CPU inexpensive mathematical functions (called “metamodels”) based, in our case on Gaussian processes [44] built from a primary set of computer code simulations. This metamodel is representative of the code in the variation domain of its uncertain parameters and presents very good prediction capabilities. In BEPU-kind analyses on PWR, several works [45,46], have introduced the use of metamodels and shown how this technique can help estimate quantiles or probability of failure in thermal-hydraulic calculations.

Only the study on the maximum clad temperatures is presented in this paper (the sodium and the wrapper temperature remaining below their safety criteria). We recall that the decoupling criterion in Operating Situation of Category 4 safety scale is that the fractile2 at 95% of this variable has to remain below 800°C. The results of the evolution of the 136 maximum clad temperatures are displayed in Figure 5. Based on a probabilistic quantification of uncertainty of these temperatures, a visualisation tool adapted from Highest Density Region (HDR) boxplots is used, following the method of [47]. HDR boxplot extends the boxplot visualization to functional data in the sense that it helps identifying a central curve (mode), zones containing a certain proportion (e.g. 50%) of most central curves and outlying curves (Fig. 5).

The first temperature peak is related to the instant of RBH drop which leads to power and core temperature decreases. This is confirmed by a GSA based on dependence measures, namely the Hilbert Schmidt Independent Criterion (HSIC) indices [48,49]. HSIC-based GSA gives the most influential variables via graphical analysis of 1D-dependencies. From the learning sample, scatter plots of the first temperature peak according to each influential inputs are drawn (Fig. 6). The estimation of 1-D conditional expectations of the output (primary effect) with the built metamodel are also plotted to extract a

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1 Inexpensive mathematical functions built from a learning sample of inputs/outputs based, for example, on polynomials, neural networks, or Gaussian processes. Once estimated, the metamodel can be used for intensive simulation, in order to perform uncertainty propagation, optimization, or calibration studies.

2 The fractile at 95% (i.e. value having 5% of probability to be exceeded) is obtained by the Wilks’ method with 95% of confidence and at the third order (i.e. taking the third most important value obtained by realizing at least 124 simulations).
possible tendency. They clearly reveals the strong decreasing monotonic and almost linear effect of the percentage of primary flow rate which triggers the RBH drop. The third main following influential variables are the model of regular head losses inside the sub-assemblies (to which is associated a large uncertainty) and then the singular head loss at the bottom of sub-assemblies.

This is also confirmed by an analysis of variance decomposition. The estimation of Sobol’ indices reveals that the percentage of primary flow rate which triggers the RBH drop explains nearly 88% of the output variance, the remaining 12% is explained by the initial core power. Furthermore, there is no significant interactions between them.

The analysis of the 136 studied scenarios reveals that 62 exceed the decoupling criterion of 800°C, that is, around 22% of cases (Fig. 7). The fractile at 95% estimated by Wilks’ formula with 95% of confidence is here equal to 880°C; thus, far above the decoupling criterion. Remember that the Wilks estimator is biased and conservative, with respect to the empirical 95%-fractile here equal to 863°C.

From this result, it is possible to review the RBH design and adjust their drop triggering so that the fractile at 95% respects the decoupling criterion. To achieve this, we consider that the built surrogate model is acceptable on all the studied domain due to its high predictivity and its linear behavior according to the RBH drop criterion. We study the evolution of the fractile at 95% of the first clad
temperature when the probability law associated with the percentage of primary flow rate, which triggers the RBH drop, is modified. More precisely, different nominal values (i.e. means) of this law are considered (cf. Tab. 5), while the laws of the other parameters remain unchanged. For each nominal value, the quantile is then estimated by intensive simulation of the surrogate model. Using this methodology, it appears that a nominal value of the criterion on the RBH drop higher than 54% of nominal flow rate leads to the respect of the decoupling criterion. It is recalled that currently this value is set at 45% (see Tab. 5). The distribution of the first temperature peak with this new criterion for RBH drop is given in Figure 8.

Fig. 7. Distribution of the 1st temperature peak.

Fig. 8. Distribution of the 1st temperature peak with the new criterion for RBH drop.

Fig. 9. Distribution of the 1st temperature peak with a nominal value at 54% for the percentage of primary flow rate which triggers the RBH drop.

maximum obtained value being 773°C. The major variables influencing this second peak are pump inertia, initial and residual core power, and then Doppler feedback.

Finally, with the lack of long term cooling, the maximum clad temperature linearly increases once the natural convection stopped at 1500 s. At term, based on results of Figure 5, we determine when the fractile at 95% of these maximum clad temperatures reacheshardly the decoupling criterion. This time is 169 h; a 7 days grace period is available to find a cooling solution. Only the residual power influences this delay length.

5 Conclusion and prospects

In this paper, the current practice of VVUQ approach application for a SFR accidental transient is described with regard to the NSA requirements. It constitutes a practical, progressively improvable approach. A scientific tool is qualified for a given version on a given scenario, 19 transients have been identified for Sodium Fast Reactor safety demonstration. Among them, the transient related to a total unprotected station blackout has been selected for a demonstration purpose. Indeed this transient is one of the most complex in this new SFR design, involving thermal stratification and natural circulation inside the main vessel and the primary loops. Thus, it requires a multiscale coupling of several thermal-hydraulic tools to correctly capture the main safety output results. The MATHYS (Multiscale ASTRID Thermal-hydraulics) tool which features a coupling of CATHARE2 at system scale, TrioMC at component scale and TrioCFDat local scale is therefore required for this study.

This paper has presented the main steps of the VVUQ application to the qualification of the MATHYS tool on the mentioned transient focusing on the main strengths and weaknesses. The steps of verification, validation (which confronts the domain of utilization to its domain of validation and/or validity) and the quantification of various sources of uncertainties (input, scenario, model…) have been described. In addition, this work presents the propagation and post-processing of a high number of uncertain parameters, enabling to review the design of the prevention hydraulic rods. Some R&D aspects have been addressed as well. These aspects are related to: a methodology to confront the tool validation domain with its utilization domain through a scaling or transposition step; the development of methods to verify the reproducibility of uncertainties propagation results; and finally, as a suggestion, of new methods to quantify the validation degree of a tool and the model uncertainties from experimental results.

Glossary

| Acronym | Description |
|---------|-------------|
| BEPU | Best Estimate Plus Uncertainty |
| CFD | Computational Fluid Dynamics |
| DHR | Direct Heat Removal |
| EMP | Electromagnetic Pump |
| GSA | Global Sensitivity Analysis |
| IET | Integral Effect Tests |
IHX  Intermediate Heat Exchangers  
IUQ  Input Uncertainty Quantification  
MCT  Maximum Cladding Temperature  
MNaT  Maximum Sodium Temperature  
NSA  Nuclear Safety Authority  
MS  Mitigation Situation  
OS  Operating Situation  
PDF  Probability Distribution Function  
PIRT  Phenomena identification and Ranking Table  
PP  Primary Pump  
PS  Prevention Situation  
PWR  Pressurized Water Reactor  
RBH  Hydraulically suspended absorber rod sub-assemblies  
SCT  Scientific Calculation Tools  
SDC  Safety Design Criteria  
SET  Separate Effect Tests  
SIT  System Integral Tests  
SFR  Sodium Fast Reactor  
TH  Thermal-hydraulics  
USBO  Unprotected Station BlackOut  
VVUQ  Verification, Validation and Uncertainty Quantification

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Author contribution statement

N. Marie conceived this application of VVUQ requirements, commonly used for PWR safety demonstration, in the framework of the SFR demonstration, organized the work and summarized the results. S. Li, A. Gerschenfeld carried out the complex multiphysic simulations and A. Marrel and M. Marquès performed the statistical part of the tasks. S. Bajard, A. Tosello, J. Perez, B. Grosjean, M. Anderhuber, C. Geffray, Y. Gorsse, G. Mauger, L. Matteo participated to the application of this VVUQ methodology, working on either the verification, validation or uncertainty quantification steps.

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