Phase-transforming metamaterial with magnetic interactions

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Solid–solid phase transformations can affect energy transduction and change material properties (e.g., superelasticity in shape memory alloys and soft elasticity in liquid crystal elastomers). Traditionally, phase-transforming materials are based on atomic- or molecular-level thermodynamic and kinetic mechanisms. Here, we develop elasto-magnetic metamaterials that display phase transformation behaviors due to nonlinear interactions between internal elastic structures and embedded, macroscopic magnetic domains. These phase transitions, similar to those in shape memory alloys and liquid crystal elastomers, have beneficial changes in strain state and mechanical properties that can drive actuations and manage overall energy transduction. The constitutive response of the elasto-magnetic metamaterial changes as the phase transitions occur, resulting in a nonmonotonic stress–strain relation that can be harnessed to enhance or mitigate energy storage and release under high-strain-rate events, such as impulsive recoil and impact. Using a Landau free energy–based predictive model, we develop a quantitative phase map that relates the geometry and magnetic interactions to the phase transformation. Our work demonstrates how controllable phase transitions in metamaterials offer performance capabilities in energy management and programmable material properties for high-rate applications.

Further advantages may be realized by combining additional fields beyond elasticity (26). Recently, the addition of field-responsive materials to metamaterials has been demonstrated to offer advantageous functionality (27–31). These demonstrations are impactful on their own, but more importantly, they introduce a broader paradigm with far-reaching implications. In particular, the combination of nonlinear fields, such as magnetic and electric, with orientationally dependent regimes of attraction and repulsion opens up the creation of “meta-atoms” that more closely reflect characteristics of atomic or molecular arrangements in materials phase structures (31). Accordingly, this counter play of nonlinear fields can be used to quantitatively define phase transitions in mechanical metamaterials composed of elastic and magnetic elements.

Here, we demonstrate the power of this paradigm by developing elasto-magnetic metamaterials that undergo phase transitions. These phase transitions, similar to enabling ones in shape memory alloys and liquid crystal elastomers, have beneficial changes in strain state and mechanical properties that can drive actuations and manage overall energy transduction. The metamaterial changes its constitutive response concurrently as the phase transitions happen, resulting in a nonmonotonic stress–strain relation. The reversible shift between the two phases significantly enhances the metamaterials’ dynamic performance, improving the

Significance

Material phase transitions offer promise for driving motion and managing high-rate energy transfer events; however, engineering conventional phase transitions at a molecular or atomic level is challenging. We overcome this challenge by coupling multiple interacting fields within a metamaterial framework. Specifically, we embed magnetic domains, with nonlinear, orientationally dependent force interactions, within elastic structures to control reversible phase transitions and program high–strain-rate deformation. The resulting high-rate energy transformations are used to enhance elastic recoil, which could be used to drive high-power motion and to quickly dampen impact loading events. The developed Landau free energy–based model for this material system broadens the impact of this advance, setting the stage for metamaterials with wide-ranging compositions, interacting fields, and engineered properties.

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energy release in dynamic recoil and mitigating the impact load-
ing. Importantly, we introduce a Landau free energy framework to model the phase transitions for the elasto-magnetic metamate-
rials, which can be extended to metamaterials with other field-
responsive materials or ones that are purely mechanical (20, 21). This framework creates opportunities based on fundamental
principles for using phase transitions to control engineering
performance at high rates.

**Results**

A schematic of the elasto-magnetic metamaterial is shown in Fig. L4. For physical demonstrations, we fabricate the metamaterials
from a polymeric sheet (PU 40A, McMaster-Carr) and cylindrical
magnets that are magnetized along the diameter (Neodymium
Magnet, McMaster-Carr). The magnet is 3.18 mm thick, 3.10
mm in diameter, and 0.18 g in weight. The thickness of the poly-
meric sheet (h) is also 3.18 mm. We laser cut (Universal Laser
System, VSL 3.5) a pattern of orthogonally aligned pores into the
polymeric sheet to create a polymeric network of “plates” con-
necting by thin “ligaments.” We define the fabricated metamate-
rial structures with the semiminor and semimajor axes \( a_0 \) and \( b_0 \) of the pores, the ligament’s width between adjacent pores, \( w_0 \).

The length of a representative unit, \( L_0 = w_0 + b_0 + a_0 \), is fixed as 6 mm. Magnets with a diameter ~3.1 mm and weight ~0.18 g

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![Figure 1](https://via.placeholder.com/150)

**Fig. 1.** Elasto-magnetic metamaterials composed of polymeric networks and interacting magnetic domains. (A) Interacting magnets are embedded in mechanical metamaterials with orthogonally aligned elliptical pores. The metamaterial structure is characterized by the ligament width, \( w_0 \), and the semi-
minor and semimajor axes, \( a_0 \) and \( b_0 \). The magnets are magnetized through the diameter, with the color representing the two poles. The ith magnet is aligned at an angle \( \theta_i \) between its magnetic moment and the y-axis. (B) Open and closed phases created by the repulsive and attractive magnetic domains, respectively (Scale bar, 10 mm). (C) Metamaterials with elliptical pores and attractive, neutral, and repulsive magnetic interactions (from Top to Bottom). (D) Metamaterials with circular pores and attractive, neutral, and repulsive magnetic interactions (from Top to Bottom).
are embedded at the center of plates such that they are constrained by frictional contact with surrounding polymer. By embedding permanent magnets in mechanical metamaterials, a rich set of mechanical properties, including buckling strain (32, 33), postbuckling stiffness (32–34), and multistability (35), have been finely tuned. Here, we reveal how magnetic domains, with nonlinear, orientationally dependent force interactions within elastic structures control reversible phase transitions and allow high-strain-rate properties to be programmed. The magnetic interactions are further programmed via the magnets’ orientations, defined by the angle between the magnetic moment and the y-axis, \( \theta_i \). We prescribe a mirror symmetry in the horizontal direction and control the magnetic interaction via the angles \( \theta_i \) and \( \theta_{i+1} \) of the neighboring magnets (Fig. 1A). An orientational parameter is defined at the configuration free from external loadings, \( Q = \cos(\theta_i)\cos(\theta_{i+1}) \), representing the relative strength of magnetic interactions and ranging from -1 to 1. The neighboring magnets are repulsive when \( Q < 0 \) and switch to an attractive interaction as \( Q > 0 \). We replace the magnets with stainless-steel cylinders (thickness \( \sim 3.18 \) mm, diameter \( \sim 3.1 \) mm, and weight \( \sim 0.18 \) g) to create metamaterials with \( Q = 0 \), labeled as neutral in Fig. 1C and D (SI Appendix, section 1 for fabrication details).

We observe two stable phases, which we refer to as “open” and “closed” regarding the state of the metamaterial pores. An open phase is induced by a strong repulsive interaction between neighboring magnetic domains with \( Q = -1 \), while with \( Q = 1 \) a closed phase develops (Fig. 1B). The phase states also depend upon the geometry of the metamaterial. For example, for elliptical pores \( a_i/b_i = 0.17 \), the elasto-magnetic metamaterials support the open phase with \( Q = 0 \) and \( -1 \) and the closed phase at \( Q = 1 \) (Fig. 1C). In contrast, circular pores \( a_i/b_i = 0.97 \) only support an open phase for all \( Q \)-values (Fig. 1D).

The equilibrium phase state can also be altered by the application of an external force. We apply a uniaxial tension to metamaterials with elliptical pores \( a_i/b_i = 0.17 \), Fig. 2A) and circular pores \( a_i/b_i = 0.97 \), Fig. 2B) under the attractive magnetic domains \( Q = 1 \). Snapshots at different deformations (marked as I, II, III, and IV) are captured for both pore shapes. The configurational changes of the two structures are remarkably different (Movies 1 and 2). A closed-to-open phase transition emerges at the top and bottom ends in the metamaterial with elliptical pores. It propagates toward the center, changing the configuration to a homogeneous open phase as the deformation increases. The sample maintains the open phase in the unloading path, ending with a fast transition to the closed phase as the magnets snap to each other when a small separation distance is reached. By contrast, the metamaterial with circular pores preserves the open phase, deforming the ligaments in response to external forces.

The phase transitions alter the relationship between the global and local strains, defined by the displacements between the neighboring magnets. The applied global strain, \( \varepsilon_g \), and the local strain for the \( i \)th magnets in the vertical direction, \( \varepsilon_i \), are the following:

\[
\varepsilon_g = \frac{y_e - y_i}{(n - 1)L_0} - 1, \quad \varepsilon_i = \frac{y_i - y_{i-1}}{y_{i+1} - y_{i-1}} - 1, \quad \text{[1]}
\]

where \( y_i \) and \( Y_i \) are the positions of the center of the \( i \)th magnet in the deformed and undeformed configuration, \( L_0 \) is the length of the representative unit of the metamaterials, and \( n = 20 \) in our experiments. We plot the evolution of the local strain \( \varepsilon_i \) as a function of the global strain \( \varepsilon_g \) for metamaterials with both elliptical (Fig. 2A) and circular (Fig. 2B) pores. As the attractive magnetic interaction creates a closed phase in elliptical pores, the global strain is negative (\( \varepsilon_g < -0.1 \)) before applying external forces. In Fig. 2A, a discontinuous change of local strain is observed between stages I and II, propagating toward the center of the sample. The traveling boundary signifies a transition between the closed and open phases. The local strain becomes uniform and changes with the global strain as the sample is dominated by the open phase (between stages II and IV).

For the circular pores in Fig. 2B, the open phase is preserved, and the global strain starts with a positive value due to the fluctuation induced by embedding the magnets into the polymer. The local strain is uniformly distributed, and it changes affinely with the global strain in the loading and unloading cycle.

The constitutive response of the elasto-magnetic metamaterial changes as the phase transitions occur. We compare the stress–strain curves for metamaterials with elliptical and circular pores (solid lines) and their elastic counterparts without magnets or stainless-steel cylinders (dashed lines, SI Appendix, Fig. S2B) in Fig. 2A and B. In materials with elliptical pores (Fig. 2A), the attractive magnetic interaction initiates an initial regime with a higher modulus than the metamaterial without magnetic domains. The transition from a closed to an open phase and the subsequent propagation of the phase interface results in a jagged state, with a plateau stress \( \sim 20 \) kPa. For an open phase, the constitutive response in elasto-magnetic metamaterials is similar to that of metamaterials without magnets due to the weak magnetic interaction at a large distance. In addition, large hysteretic is observed in elasto-magnetic metamaterials with elliptical pores (Fig. 2B), which is negligible in the mechanical metamaterials or magnetic interactions alone (SI Appendix, Fig. S2). This is related to the differences in the phase transitions between the loading and unloading cycles. In circular pores (Fig. 2B), the magnetic interaction is weak at the open phase. The ligament’s constitutive response results in an initial regime similar to mechanical metamaterials without the phase transitions. The softening observed in the constitutive response at large strain (stage II) is mostly due to the debonding between the polymer and the magnets (SI Appendix, Fig. S7), contributing to the enhanced hysteresis in elasto-magnetic metamaterials with circular pores.

To further explore the relationship between the structure and constitutive response, we measure the loading and unloading response for materials as a function of magnetic interaction parameter \( Q \), pore shape \( a_i/b_i \), and ligament thickness \( w_0 \) (Fig. 2C). For example, for elasto-magnetic metamaterials with an attractive magnetic interaction \( Q > 0 \), an elliptical pore shape \( a_i/b_i < 0 \) with relative compliant responses at small strain and a relatively thin ligament \( w_0 < L_0 \), the phase transitions are induced, thus creating the stress plateau in loading and an enhanced hysteretic response upon unloading. A mathematical framework to describe the materials structures prone to these transitions would be advantageous for systematically programming materials with prescribed energy dissipative and recovery modes.

To understand how the internal geometry and the magnetic interaction affect the phase transitions and the constitutive responses in elasto-magnetic metamaterials, we develop an analytical model described in Fig. 3A. Following Landau’s analysis of phase transitions (36), we construct a Landau free energy \( F_L \), which is the effective Hamiltonian of the system (SI Appendix, section 3), based on local equilibrium:

\[
L_0h[\sigma_i(\varepsilon_{i+1}) - \sigma_i(\varepsilon_i)] - G_mQ^{1/2}(\delta_0 + u_{i+1} - u_i)^{-4} - (\delta_0 + u_i - u_{i-1})^{-4} = 0, \quad \text{[2]}
\]

where \( u_i \) is the displacement of the \( i \)th magnet; \( \sigma_i(\varepsilon_i) \) is the stress–strain relation of the mechanical metamaterials without magnetic domains; \( G_m \) is the coefficient for the magnetic interaction; \( \delta_0 \) is the center-to-center distance between two neighboring magnets in the closed phase; and \( h \) is the thickness of the sample. The constitutive responses of the mechanical
metamaterials and the magnets are adopted from the measurements shown in SI Appendix, Fig. S2. We trade the details of the “microscopic” degree of freedom (e.g., the displacement of each magnet $u_i$) to a coarse-grained continuum field $\varepsilon_i$, which is a continuous limit of $u_i$ in the “macroscopic” scale and serves as the order parameter for the phase transitions. We can rewrite the equilibrium equation (Eq. 2) to the continuum limit and calculate the Hamiltonian of the elasto-magnetic metamaterials (SI Appendix, section 3) for details) per-unit volume ($H(\varepsilon, d\varepsilon/dy)$) under the external force $f_p$ as the following:

$$H(\varepsilon, d\varepsilon/dy) = \frac{1}{2} \alpha_m (d\varepsilon/dy)^2 + \frac{1}{2} k_m \varepsilon^2 - \frac{1}{6} \beta_m \varepsilon^3 + \int_{0}^{\varepsilon} \sigma_s(y)dy - f_p \varepsilon,$$

where $\alpha_m = L_0^2 G_m Q/3h \delta_0^2$, $k_m = 4G_m Q/5h \delta_0^5$, $\beta_m = 20L_0G_m Q/21h \delta_0^7$, and $\gamma$ is the dummy variable for the integration. The closed and open correspond to the order parameters $\varepsilon < 0$ and $\varepsilon > 0$, respectively. We focus on the vicinity of the phase transitions, where the Landau free energy is expanded as an analytical polynomial function of $\varepsilon \sim 0$. To a first-order approximation, we expressed the stress–strain relation in the mechanical metamaterials as $\sigma_s(\varepsilon) = C_1 \varepsilon + C_3 \varepsilon^3$, which captures the sign change in stresses as the deformation switches from tension to compression. Here, we drop the even order term in $\sigma_s$ assuming the strain energy is symmetric with strain $\varepsilon$ under tension and compression. The dependence of the parameters $C_1$ and $C_3$ upon metamaterial geometry is fitted to the experiments through linear functions for simplicity. We note that the accuracy of the stress–strain relation can be improved by adding more terms to the fitting functions; however, the underlying symmetry and the physics at phase transitions is captured by the Landau free energy. In the mechanical metamaterials, the Landau free energy density is written as the following:

$$F_L = -B_1 \varepsilon + \frac{1}{2} B_2 \varepsilon^2 - \frac{1}{3} B_3 \varepsilon^3 + \frac{1}{4} B_4 \varepsilon^4, \quad [4]$$

where $B_1 = f_p$, $B_2 = (k_m + C_1)$, $B_3 = \beta_m/2$, and $B_4 = C_3$. We neglect the term $\alpha_m (d\varepsilon/dy)^2/2$, as it is positive and serves as an energy penalty to keep $\varepsilon(y)$ smooth without forming two phases.
alternatively. Remarkably, the Landau free energy for elasto-magnetic metamaterials under external loading is similar to liquid crystal elastomers undergoing the nematic-to-isotropic phase transitions under external fields (37, 38). Based on the Landau-de Gennes theory, we expect the closed-to-open phase transitions to echo the first-order phase transitions observed in liquid crystal elastomers (39). Minimizing Eq. 4 to ε and normalizing by the critical coefficient values (40), the equilibrium condition for different phases is the following:

$$B_2/B_2^c = -\frac{1}{2} \left( \frac{\epsilon}{\epsilon_{cp}} \right)^2 + \frac{3}{2} \left( \frac{\epsilon}{\epsilon_{cp}} \right) + \frac{1}{2} \frac{f_p}{f_p \sigma_{cp}} \left( \frac{\epsilon}{\epsilon_{cp}} \right)^{-1},$$

where $\epsilon_{cp} = B_1/3B_4$, $B_2^c = B_1^c/3B_4$, and $\sigma_{cp} = B_1^c/27B_4^c$ are the mechanical critical points satisfying $F_1^c(\epsilon) = F_1^c(\epsilon) = F_1^c(\epsilon) = 0$, and $B_2^c = 2B_2^c/3$. In Fig. 3B, the scaled strains $\epsilon/\epsilon_{cp}$ are plotted as a function of $B_2/B_2^c$, which is the reduced parameter for the coupling between the magnetic interaction and the elastic constitutive response, with different external forces $f_p/\sigma_{cp}$. An open phase ($\epsilon/\epsilon_{cp} > 1$) is reached with a repulsive or weakly attractive magnetic interaction, as $B_2/B_2^c < 1$. When the attractive magnetic interaction increases ($B_2/B_2^c > 1$), a closed phase ($\epsilon/\epsilon_{cp} < 1$) is favored. Without external force ($f_p = 0$), the absolute minimum of the free energy density is located at $\epsilon = 0$ for strongly attractive magnets. As the interactions weaken, a metastable minimum with $\epsilon_m > 0$ appears. At $B_2 = B_2^c$, the absolute minimum at $\epsilon = 0$ jumps discontinuously to $\epsilon_m$, causing the first-order phase transitions (Fig. 3B, Inset). The points around the transition indicate the coexistence of both phases (arrows in Fig. 3B). For an external force $f_p > 0$, the closed pore phase with $\epsilon = 0$ no longer exists, and the strain after the phase transitions decreases. The strains at phase coexistence are related to the external force, $\epsilon_c = \epsilon_{cp}(1 \pm \sqrt{1 - f_p/\sigma_{cp}})$, and these conditions are plotted with dashed lines for different external forces in Fig. 3B. As the external force increases, the discontinuous jumping of the strain in the phase transitions reduces. The closed-to-open phase transformation is of second order when $f_p = \sigma_{cp}$. The phase transitions disappear as $f_p > \sigma_{cp}$, as
observed in Fig. 2A, when the stress is larger than the plateau stress. We also mark the experimental data for phase coexistence with solid circles in Fig. 3B, where the metamaterials experience a closed-to-open phase transition shown in Fig. 2A (SI Appendix, section 4). The Landau free energy analysis captures the discontinuous phase transitions for the elasto-magnetic metamaterials, agreeing with the experiments.

We construct a phase diagram to compare our model predictions with the experiments and illustrate how internal structures and magnetic interactions control phases in elasto-magnetic metamaterials. The critical condition for the first-order phase transitions in elasto-magnetic metamaterials is determined with zero external force, $f_p = 0$.

$$2B^2 - 9B^2B_4 = 0. \quad [6]$$

In Fig. 3 C and D, we plot the phase diagram for a fixed magnetic moment direction ($Q = 1$) and a fixed ligament width ($w_0/L_0 = 0.16$), respectively. The scaled magnetic strength $D_{cm}/(h_bL_0^2) = 0.025$ for the Neodymium magnet is determined by its magnetic moment and the magnetic permeability (SI Appendix, section 2). As shown in Fig. 3C, under a fixed magnet orientation ($Q = 1$), the metamaterials show a dual phase (blue symbols) with elliptical pore shapes and a small ligament thickness ($w_0/L_0 < 0.25$). On the other hand, the single open phase (red symbols) is observed for metamaterials with circular pore shapes and thick ligaments. Eq. 6 delineates the phase boundary (blue line) based on the Landau free energy, which is accurate for elliptical pores with $a_0/b_0 < 0.5$. However, it overestimates the critical conditions for phase transitions as $a_0/b_0$ approaches 1.

Deviation from the Landau free energy is observed in elasto-magnetic metamaterials with circular pores. In these cases, the slender ligament connecting the neighboring circular pores buckles to form a closed phase instead of bending. To account for this alternative deformation path, we adopt the Euler buckling criterion and predict compressive load for the ligament buckling as $F_{cr} = \pi^2C_b/L_0^2$. Here, we model the ligament as a simply supported Euler beam with length $L_0$ and bending stiffness $C_b$ (23). The applied compressive force in the ligament without external loading is dictated by the strength of the magnetic interaction: $F_m = G_mQ/L_0^2$. The phase boundary based on ligament buckling is determined by $F_{cr} = F_m$, shown with a red line in Fig. 3C, which intersects with the line from Eq. 6 at $a_0/b_0 = 0.53$. The region enclosed by both criteria (solid lines) in the phase diagram represents the conditions for metamaterials with a dual phase that supports phase transitions. As indicated by comparing with the experimental results, the phase diagram constructed by the Landau free energy and ligament buckling captures the boundary between the dual and single phase in elasto-magnetic metamaterials (Fig. 3 C and D).

We demonstrate the capacities enabled by the phase transformation in high-rate deformation through dynamic recoil and impact experiments. As shown in Fig.4A, the recoil of vertically hung metamaterials without any external guiding constraints is studied. Out-of-plane bending is suppressed as the metamaterials thickness ($h$) is much larger than ligament width, $h \sim 3w_0$. High-speed images (Photron Fastcam APX RS, 10,000 frames per second [fps]) of the recoiling metamaterials with different magnetic interactions are shown in Fig. 4A. The metamaterials ($w_0 = 1$ mm and $a_0 = 0.17b_0$) are stretched to the same deformed length with $\varepsilon_g = 0.2$, and recoilling is initiated by a trigger at time $t = 0$ ms along the $y$-direction. We track the position of the magnet via markers placed in the metamaterials (Fig. 4A). The positions corresponding to the color markers in metamaterials with different magnetic interactions ($Q = 1, 0,$ and $-1$) are measured against the recoil time (SI Appendix, Fig. S17). The recoil velocities based on the time derivative of the displacements are compared in Fig. 4B. The repulsive ($Q = -1$) and neutral interactions ($Q = 0$) share similar dynamic responses as they are mainly powered by the ligaments’ elastic deformation (SI Appendix, section 5). The repulsive magnetic interaction also enforces an opposing force in the recoiling direction, reducing the elastic recoil velocity by $\sim 30\%$ compared to the recoil for metamaterials with $Q = 0$. By contrast, the metamaterials with attractive interactions experience a phase transformation during recoil, leading to a rapid collapse of the pores (Movie S3). The propagation of the phase transitions, superimposed with the elastic recoil, nearly doubles the elastic recoil velocity. For the metamaterial with circular pores ($w_0 = 1$ mm and $a_0 = 0.97b_0$), which predictably only supports the open phase even with the attractive magnetic interaction ($Q = 1$), the effect of the magnetic interactions on the recoil velocity is much smaller, nearly less than $10\%$ (SI Appendix, Fig. S18). Therefore, the propagation of the phase transitions in the metamaterials is responsible for the enhanced high-strain-rate energy release in dynamic recoil.

While the programmed phase transitions in elastic recoil harness latent energy to access enhanced recoil velocities, programmed phase transitions can also enhance energy dissipation during high-speed impact events. We demonstrate this through a simple experiment designed to measure the damping response of the metamaterial with an impacting mass (Fig. 4C). The mass is accelerated by launching it from a pre-determined height. The attached metamaterial ($w_0 = 1$ mm and $a_0 = 0.17b_0$) stops its fall through stretching (Fig. 4C and SI Appendix, section 2 for details of experiments). We track the dynamic response of the free-falling mass and the metamaterial through high-speed imaging (1,000 fps). For the metamaterials without magnetic interactions ($Q = 0$), the system oscillates with the free-falling mass, resembling a damped mass-spring vibration (41), where the impact energy is slowly dissipated (SI Appendix, section 5 and Movie S4). The free-falling mass impact stretches the metamaterial with attractive magnetic interactions ($Q = 1$), but it ceases vibration over a much shorter timescale, indicating significant dampening capabilities (SI Appendix, section 5 and Movie S5). As shown in Fig. 4C, part of the elasto-magnetic metamaterials undergoes a closed-to-open phase transition. The vibrations here only last for a few periods, accompanying the emergence of the open phase (at $t = 0.5$ s). The closed-to-open phase transitions govern the subsequent deformation, resulting in an almost quasistatic motion, which is heavily damped. The displacement of an 80-g free-falling mass (or the extension of the metamaterial) and the corresponding velocity are plotted in Fig. 4 D and E.

To further explore the damping mechanism, we perform impact experiments for elasto-magnetic metamaterials with different falling weights, ranging from 60 to 120 g. The energy transfer in the impact is characterized based on the high-speed images, which measures the ratio between the kinetic energy in the mass $E_k$ (through the vibrational velocity) and the gravity potential $E_{impact}$ (refer to the maximum extension) for different weights (SI Appendix, Figs. S19B and S20B). As shown in Fig. 4F, more than 40% of the total energy is converted to kinetic energy after impact, leading to high-frequency vibrations that take 0.7 s to dissipate for metamaterials without magnetic interactions ($Q = 0$). The energy conversion event is governed by the damped oscillation, whose period is about 0.1 s for different falling weights, while the dissipation increases with the impact velocity as the weight grows. For metamaterials with attractive magnetic interactions ($Q = 1$), the vibration decays rapidly in 0.2 s, with less than 20% of the impact energy converted to kinetic energy (Fig. 4G). The rapid absorption of the impact energy relies on the phase transitions and not on the attractive magnetic interactions, as confirmed with experiments on elasto-magnetic metamaterials with circular pores (SI Appendix, section 5). In these circular pore metamaterials with $Q = 1$, SI Appendix.
the damped harmonic vibration upon impact is similar to the metamaterials with $Q = 0$ (SI Appendix, Fig. S21).

Compared to the traditional impact absorption that relies on internal friction and viscoelastic material responses, the damping mechanism in elasto-magnetic metamaterials offers multiple energy barriers through the phase transitions that are activated upon impact. We illustrate the proposed mechanism in the inset of Fig. 4G. The movements of the sphere represent the vibration after impact. Additional energy barriers emerge as the metamaterials transform from a closed to an open phase. The modulated energy landscape dramatically reduces the maximum impact velocity, leading to fast and efficient damping compared to traditional materials (10, 22). While the current phase diagram framework provides insight into how to design an appropriate metamaterial for achieving these damping responses, further research is required to quantitatively predict the dynamic performance. In particular, inertial and multiphase wave propagation dynamics must be incorporated within the phase framework.

Conclusions

In conclusion, we demonstrate programmable solid–solid phase transitions through metamaterials that integrate elastomers with internal structures and magnetic domains. By controlling the elastic and magnetic interactions, we engineer two distinct phases—the closed and open phases—in the deforming metamaterials and show that capabilities for energy storage and management are introduced by crossing through the phase boundary. A Landau free energy–based model predicts the design space for metamaterial geometry and magnetic interactions to support phase transitions. We demonstrate that magnetic interactions, instead of only elasticity [e.g., buckling (21) or suppression of internal rotations (20)], can control the coefficients in the Landau free energy and modulate the phase transitions. The coexistence of the closed and open phases in metamaterials and their transition induce a stress plateau during mechanical deformation with enhanced energy storage and mitigation capacity. The reversible phase transitions under external loading enable the programming of dynamic performance in high–strain-rate applications, such as elastic recoil and free-falling mass impact. In dynamic recoil, the coupling between the elastic and magnetic response enhances the recoil velocity. This improved dynamic performance is anticipated to help engineered systems achieve high-power actuation by harnessing latent energy associated with the phase transitions. The phase transitions also provide a different approach for energy mitigation. Crossing the phase boundary when the metamaterials are subjected to an impact can dissipate a large amount of energy, modulated by the energy landscape in the phase transitions. This capability was demonstrated directly by controlling the dampening of a high-rate impact loading event. The reversible and programmable phase
transitions enabled in the elasto-magnetic metamaterials can pave the way for future research to generate phase structures with mesoscale design, going beyond the traditional solid-to-solid phase transitions at the molecular level. The metamaterials developed in the current study provide a platform for high-performance materials in energy storage and release, achieving programmable material properties and impacting the design of robotic systems.

**Materials and Methods**

Details of fabrication of metamaterials are described in *SI Appendix*, section 1. The protocol for experiments and additional experimental data are provided in *SI Appendix*, sections 2 and 5. Derivations and discussions of theoretical models about the phase diagram of elasto-magnetic metamaterials are presented in *SI Appendix*, sections 3 and 4.

**Data Availability.** All study data are included in the article and/or supporting information.

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