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Reconciliation of Experiments and Theory on Transport Properties of Iron and the Geodynamo

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We measure the electrical resistivity of hcp iron up to ~170 GPa and ~3000 K using a four-probe van der Pauw method coupled with homogeneous flattop laser heating in a DAC, and compute its electrical and thermal conductivity by first-principles molecular dynamics including electron-phonon and electron-electron scattering. We find that the measured resistivity of hcp iron increases almost linearly with temperature, and is consistent with our computations. The results constrain the resistivity and thermal conductivity of hcp iron to ~80 ± 5 μΩ cm and ~100 ± 10 W m⁻¹ K⁻¹, respectively, at conditions near the core-mantle boundary. Our results indicate an adiabatic heat flow of ~10 ± 1 TW out of the core, supporting a present-day geodynamo driven by thermal and compositional convection.

Earth’s core works like a heat engine through heat transfer from the cooling and freezing of the liquid iron core, which powers the present-day geodynamo, mantle convection, and plate tectonics [1,2]. Paleomagnetic records indicate that the geodynamo has been active for at least 3.4 Gyr [3]. The geodynamo was long believed to be driven by primordial convective motions in the deep Earth, which were powered by core formation: the higher the electrical and thermal conductivities are, the faster Earth’s core cools, and the younger the inner core [1].

Several experimental studies have been conducted at high P-T conditions, but measurements of the transport properties of Fe using different methods came to dramatically contradictory results [5,14–17]. The current estimate of thermal conductivity of iron under CMB conditions varies by a factor of ~6 in laser-heated DAC experiments (summarized in Table S1 [18], which includes Refs. [5–9,14,15,19–27]); this translates into the CMB heat flux of 4–20 TW. A very high thermal conductivity of 226±17 W m⁻¹ K⁻¹ in hcp Fe at the topmost outer core was derived via the Wiedemann-Franz law (κ = LT/ρ) through electrical resistivity (ρ) measurements [14,17]. However, direct thermal conductivity measurements of hcp Fe gave a low thermal conductivity of 33 ± 7 Wm⁻¹ K⁻¹ near the CMB [15,28,29]. New theoretical calculations show that both electron-phonon and electron-electron scatterings contribute to the thermal conductivity of iron, and give a value of 97 ± 10 W m⁻¹ K⁻¹ for hcp Fe at the CMB conditions, and modify the Wiedemann-Franz law [20]. Electron correlations beyond density functional theory (DFT) increase the resistivity by about 35% at Earth’s core conditions over the conventional DFT values, and reduce the thermal conductivity by a similar factor [20]. The computed thermal conductivity is between those inferred from the experimental thermal conductivity and electrical resistivity measurements.
The discrepancy [30,31] between the thermal conductivity and resistivity measurements may arise from temperature gradients in the laser-heated samples, sample deformation and textures, probe geometry, and the breakdown of ideal Wiedemann-Franz law (see Supplemental Material [18], which includes Refs. [7,8,14,17,20,32–34]). Uncertain thermal conductivity of the core may result in a big difference in our understanding of the thermal history of the core and its geodynamo [35,36]. Thus, further improved and integrated experimental measurements and theoretical studies on the transport properties of Fe at high P-T are needed.

We used a modified four-probe van der Pauw method [37] to reliably measure the electrical resistivity of hcp Fe at high P-T in a double-side laser-heated DAC with two flattop laser beams [38] (see Supplemental Material [18,39]). An iron sample (~2 μm thick) was shaped into a uniform Greek cross sheet with a circular region of ~6 μm at the central cross area (cloverleaf) using a focused ion beam (FIB) [Fig. 1(a)]. The cross sheet has four arms with a length of ~70 μm, which act as internal electrode wires [Fig. 1(b)]. The arms were connected to four external Pt leads. The heart area of the cloverleaf matches well with a finely focused laser-heating spot (~10 μm, Fig. 1(c)). Our samples have a smaller width than the laser spot, ensuring homogeneous flattop heating with uniform temperature distributions on both sides of the sample. The Greek cross sheet with a diameter varied from ~6 μm to hundreds of micrometers has been proved to be a valid van der Pauw test structure by theory and experiment [37,40]. The sample assembly also avoids contact resistance and contamination from possible alloying between Pt leads and Fe sample.

We first measured the electrical resistivity of hcp Fe up to ~140 GPa at room temperature. The pressures and volumes were determined by the thermal equation of state [41] of hcp Fe from in situ synchrotron x-ray diffraction at high P-T (example patterns in Fig. S1 in the Supplemental Material [18]) during the resistivity measurements at GSECARS, Advanced Photon Source. The resistivity in hcp Fe decreases with increasing pressure (Fig. S2 [18]), consistent with previous studies [5,16]. We then measured resistivity at ~105 GPa with increasing temperature up to ~3000 K (Fig. 2); the resistivity increases with increasing temperature almost linearly, with an intercept of ~4.8 μΩ cm at room temperature. The temperature dependence of our data is very different from the result of previous experiments [14], which showed a significant reduction of resistivity with temperature (Fig. 2). Our measured resistivity is around 1.6 times higher than Ref. [14] up to 3000 K at ~105 GPa. This difference is likely due to the temperature gradient and sample geometry in the earlier experiments. We tested this at ~74 GPa by introducing an artificial temperature gradient, in which we heated one corner of a relatively large sample of ~15 μm in diameter compared to the focused laser spot of ~10 μm (Fig. S3a in the Supplemental Material [18]). When the laser spot size and position did not match well with the sample, we observed strong resistivity saturation similar to what was reported in Ref. [14] (Fig. S3b in the Supplemental Material [18]). The details on the temperature gradient issue are discussed in the Supplemental Material [18].

We carried out additional high-temperature experiments using homogeneous laser-heated DACs up to ~3000 K from ~82 to ~165 GPa, where only hcp Fe was observed (Fig. S4 [18]). We analyzed the temperature distribution on a sample with ~6 μm width at ~2380 K and ~142 GPa. It shows a very homogeneous temperature in a width of ~8 μm (Fig. S5 in the Supplemental Material [18]), which matched well with the sample size. The measured resistivities at 82, 133, 142, and 165 GPa are shown in Figs. S6a–S6d in the Supplemental Material [18], respectively. We found that the resistivity for all these well-heated Fe samples in our experiments increased quasilinearly with increasing temperatures up to ~3000 K in experiments. The results could be fitted well with the Bloch-Grüneisen formula at the measured P-T range (solid blue curves, Fig. 2) (see Supplemental Material and Table S2 [18,42]).

We compare our experimental data with computations of transport properties that include e-ph and e-e scattering based on first-principles lattice dynamics and density functional perturbation theory (DFPT) [20], and also with our new results using first-principles molecular dynamics (FPMD) (see Supplemental Material and Fig. S7 [18],

![Image](image_url)
FIG. 2. Measured and calculated resistivity of hcp Fe at ∼105 GPa with increasing temperature up to ∼2980 K in a laser-heated DAC. The pressure of 105 GPa was determined at ambient temperature by x-ray diffraction. At ∼2980 K, the pressure is about 117 GPa according to the thermal equation of state of hcp Fe [41]. Our measurements are compared with the current calculations that considered both e-ph and e-e contributions by DFPT + DMFT (Ref. [20], solid squares) and new calculations by FPMD + DMFT (this study, solid green star), and also compared with previously measured resistivity [14] (open circles) and calculations considered only e-ph contribution (Ref. [20], open red squares). e-ph is the electron-phonon contribution of resistivity calculated by DFPT with inelastic Boltzmann theory, e-e is the electron-electron contribution of resistivity, and “sat” is resistivity saturation effects for the e-ph scattering. The red dashed line through the calculated resistivity is a guide to the eye. The solid blue curve is fitted using the Bloch-Grüneisen formula for the measured resistivity. The black short dashed line represents the saturated resistivity fitted by a shunt resistor model in Ref. [14].

which includes Refs. [43,44]). In the former computations, the e-ph contribution was computed using the inelastic Boltzmann transport equation [45] and DFPT; and the e-e contribution was obtained using density functional theory and dynamical mean field theory (DFT + DMFT) [46,47]. Now we have performed further FPMD computations, and evaluated transport properties using DFT + DMFT. Any saturation effects are included automatically and naturally in the FPMD (see Fig. S7 and discussion in Supplemental Material [18], which includes Refs. [48–54]). Neither the present calculations, nor those in Ref. [20] use fitting to data to obtain saturation effects, but the previous work relied on a model of saturation based on mean-free path and assumed Matthiessen’s rule, that e-e and e-ph scattering can be computed separately and added. Our new measurements are consistent with the computed resistivities by DFPT and DMFT (Ref. [20]) (solid red squares and dashed red line in Fig. 2). In addition, the calculation is also consistent with a model that assumes a Bloch-Grüneisen form fit to our data (Fig. 2). Using separately computed e-ph and e-e scattering with a model for saturation effects in Ref. [20] gives about 10% higher resistivity than that extrapolated from the Bloch-Grüneisen formula up to 3500 K. Using FPMD with DFT and DMFT we obtain new results that agree perfectly with our new experimental results for hcp Fe in Fig. 2 (solid green star). It is encouraging that a very different theoretical technique based on FPMD and very different assumptions agrees well with first-principles lattice dynamics results that include a model for resistivity saturation. The measured resistivity of hcp Fe is also compared with the calculated resistivity contributed only by e-ph scattering (Ref. [20], open red squares and dash-dotted red line in Fig. 2). One can see that the e-e contribution to the resistivity is less than 10% at ∼1500 K, but it reaches above ∼20% to 3000 K at ∼105 GPa, indicating a non-negligible effect of e-e scattering on the resistivity of hcp Fe by both the experiments and theories, especially at high temperatures. The effects on thermal conductivity are larger, as discussed in Ref. [20], indicating a nonideal Lorenz number at high P-T.

To estimate transport properties for Earth’s core, we extrapolated the resistivity of hcp Fe up to 4000 K above 133 GPa by the Bloch-Grüneisen formula [Fig. 3(a) and Fig. S6 [18]]. The electrical resistivity is found to be ∼80 ± 5 μΩ cm in hcp Fe near CMB conditions (∼136 GPa and 4000 K). Compared with the previous data by DAC experiments (Ref. [14]), our results show about 1.5 to 2 times higher resistivity at the relevant conditions of the outer core [Fig. 3(a)]. Our determined resistivity of hcp Fe at ∼140 GPa and ∼3000 K generally agree with the previous shock experiment by Ref. [11] but significantly smaller than the one by Ref. [10] [Fig. 3(a)]. Future shock experiments are needed to find out the reason for the large difference in these studies. Based on the computed resistivity and thermal conductivity of hcp Fe at the CMB conditions (Ref. [20]), the Lorenz number is estimated to be (∼(2.0−2.1)×10−8 WΩ K−2, which is ∼20% lower than the ideal value (Supplemental Material and Fig. S8 [18], which includes Refs. [55–57]). Comparing the Lorenz number with that obtained by Ref. [7] [open diamonds in Fig. 3(b)] shows that our finding is ∼10% lower than that calculated from molecular dynamics simulation without e-e scattering for Fe. We convert the experimental resistivity data for hcp Fe at high P-T to the thermal conductivity using the computed Lorenz number in the Wiedemann-Franz law, and obtain a thermal conductivity significantly lower than the previous estimates by Ref. [14] that used the ideal Lorenz number (2.44 × 10−8 WΩ K−2) [Fig. 3(b)]. At about 136 GPa and 4000 K, at near CMB conditions, we find that the thermal conductivity in hcp Fe is around 100 ± 10 W m−1 K−1. Our values are still somewhat higher than the results measured by Ref. [15] through direct observations of heat pulse in hot dense hcp Fe, and deviate more with their extrapolated values with increasing pressure. Thus, it seems that the previous electrical conductivity was too high, and the previous thermal conductivity was too low.
Our theory and experiment results fall between the above two previous studies [14,15]. The effect of hcp Fe texture in a DAC on the electrical anisotropy is estimated to be approximately 10%, whereas recent calculations show the electrical anisotropy between c and a axis to be ∼26% at Earth’s core P-T conditions [20]. A recent study reported approximately 30% anisotropy in modeled thermal conductivity of textured hcp Fe samples at 20–45 GPa and 300 K [58], which are generally consistent with the first-principles estimates (Ref. [20]). A very large anisotropy of $k_{\text{c}}/k_{\text{a}} = 3$ for hcp Fe at relevant core P-T conditions was suggested by an extrapolation of the limited data to Earth’s core, but the uncertainty is too large to be credible for our understanding of the core geodynamo [58]. Therefore, the discrepancy between this study and previous experimental values cannot be simply explained by textures of hcp Fe crystals (see Supplemental Material [18], which includes Refs. [59–62]).

The outer core is liquid so the effects of melting on the thermal conductivity should be considered. Previous high P-T experiments in heated multi-anvil apparatuses show a ∼5%–10% resistivity increase upon melting from fcc Fe below ∼10 GPa [25,26,63,64]. It is still difficult to directly measure the resistivity of liquid Fe in experiments at core conditions so that we have to estimate the effects of the melting of hcp Fe. The recently computed resistivity and thermal conductivity considered the scattering of electrons from both atomic motions (e-ph) and electrons (e-e) shows a 7%–10% increase in resistivity or decrease in thermal conductivity upon melting from hcp structure at 4000–5000 K and ∼145 GPa (Ref. [20]), which is slightly lower than previous calculations of ∼15% change, which only considered e-ph contributions (Ref. [24]). Therefore, if we use a value of ∼10% increase of resistivity after melting, the thermal conductivity of liquid Fe would be around $90 \pm 15$ W m$^{-1}$ K$^{-1}$ at the relevant condition of the CMB [solid red star, Fig. 3(b)].

Earth’s outer core contains ∼8 wt % light elements, such as Si, O, S, and C [65], and about 5 wt % Ni, Si, S, and O are proposed to be the most likely major light element(s) based on recent studies [66,67]. Each weight percent of Si, S, and O light elements could reduce the thermal conductivity by 2%–4% near CMB conditions in recent calculations and high-pressure experiments [7,16,27,68]. Thus, an additional 20%–30% decrease in the thermal conductivity is reasonable by the light element impurities of 8–10 wt % for an Fe-Si-O/Fe-S-O outer core. Consequently, the thermal conductivity for liquid Fe alloy at the CMB conditions ($\kappa_{\text{CMB}}$) would be $70 \pm 10$ W m$^{-1}$ K$^{-1}$, which is 30%–50% smaller than previous DFT computations (∼100–140 W m$^{-1}$ K$^{-1}$) [7,8]. We should note that future collaborative experimental and theoretical studies with smaller uncertainties on melting and alloying effects of Ni and light elements on the thermal conductivity of iron at realistic outer core P-T conditions are needed to more accurately interrogate the heat flux paradox.
With taking a CMB temperature of $3.900 \pm 200$ K and using results of recent studies on a Si-rich Fe alloy [69], the isentropic heat conduction down the outer core adiabat would be further constrained to be $\sim 10 \pm 1$ TW (Supplemental Material [18,70,71]), which contributes $\sim 22\%$ in Earth’s global interior heat loss (46 $\pm$ 3 TW) [2]. The adiabatic heat flow of $\sim 10 \pm 1$ TW near the topmost outer core in this study is comparable to the recent heat flow estimates (7–13 TW) from the lowermost mantle, which was estimated from the reported lattice thermal conductivity of silicates and oxides ($\sim 8$–$15$ W m$^{-1}$ K$^{-1}$) at the lowermost mantle conditions (Table S1 [18], which includes Refs. [2,10,72–79]). According to a recent model of heat budget in the core [13], our estimated CMB thermal heat flux of $\sim 10$ TW can be mainly contributed from a secular cooling associated with the heat capacity of the core ($\sim 4.8$ TW), the latent heat associated with the freezing of the inner core ($\sim 3.3$ TW), and the gravitational energy associated with the light element partitioning across the inner-core boundary ($\sim 2.0$ TW) (Fig. S11 and Supplemental Material [18,80,81]). Both thermal and compositional convections play an equally important role in driving the present-day geodynamo. In addition, our determined thermal conductivity at the topmost core ($\sim 70$ W m$^{-1}$ K$^{-1}$) supports a geodynamo driven by thermal convection over Earth’s history [36] and therefore solved the “core paradox” raised by Olson [82].

Based on the recent modeling of the core thermal evolution [4,5] and the thermal heat flux of 10 TW across the CMB, the age of the inner core is constrained to be 1.0–1.3 Gyr. This is significantly lower than some estimates of 3.5–4.2 Gyr [6,15], but higher than recent claims of less than $\sim 0.7$ Gyr [14]. Our study points to a 30%–50% reduction in the thermal conductivity of iron alloy as compared with previous studies ($\sim 100$–$140$ W m$^{-1}$ K$^{-1}$) at near CMB conditions [5,7,8,14], which could translate into a difference in the estimated inner-core age as large as a factor of 2. We should note that the estimation of the inner core age also depends on the thermal conductivity of the lowermost mantle materials and radioactivity in the core [13]. An increase in both average field strength and variability of Earth’s palaeomagnetic field was observed to occur between 1.0 to 1.5 Gyr [83]. Our results would provide an explanation for the change of the observed palaeomagnetic field by the nucleation of Earth’s inner core. However, recent magnetic evidence from samples of the $\sim 0.565$ Gyr Sept-Îles intrusive suite shows an anomalous palaeomagnetic field during the Ediacaran period [84], indicating a young inner core of 0.5–0.7 Gyr. Therefore, further interrogations between mineral physics, geodynamics, and paleomagnetism are needed to resolve this discrepancy.

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