Diagnostic performance of virtual fractional flow reserve derived from routine coronary angiography using segmentation free reduced order (1-dimensional) flow modelling

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Abstract

Introduction: Fractional flow reserve (FFR) improves assessment of the physiological significance of coronary lesions compared with conventional angiography. However, it is an invasive investigation. We tested the performance of a virtual FFR (1D-vFFR) using routine angiographic images and a rapidly performed reduced order computational model.

Methods: Quantitative coronary angiography (QCA) was performed in 102 with coronary lesions assessed by invasive FFR. A 1D-vFFR for each lesion was created using reduced order (one-dimensional) computational flow modelling derived from conventional angiographic images and patient specific estimates of coronary flow. The diagnostic accuracy of 1D-vFFR and QCA derived stenosis was compared against the gold standard of invasive FFR using area under the receiver operator characteristic curve (AUC).

Results: QCA revealed the mean coronary stenosis diameter was 44% ± 12% and lesion length 13 ± 7 mm. Following angiography calculation of the 1DvFFR took less than one minute. Coronary stenosis (QCA) had a significant but weak correlation with FFR (r = −0.2, p = 0.04) and poor diagnostic performance to identify lesions with FFR <0.80 (AUC 0.39, p = 0.09), (sensitivity – 58% and specificity – 26% at a QCA stenosis of 50%). In contrast, 1D-vFFR had a better correlation with FFR (r = 0.32, p = 0.01) and significantly better diagnostic performance (AUC 0.67, p = 0.007), (sensitivity – 92% and specificity - 29% at a 1D-vFFR of 0.7).

Conclusions: 1D-vFFR improves the determination of functionally significant coronary lesions compared with conventional angiography without requiring a pressure-wire or hyperaemia induction. It is fast enough to influence immediate clinical decision-making but requires further clinical evaluation.

Keywords
Coronary imaging: angiography/ultrasound/Doppler/CC, catheter-based coronary interventions: stents, cardiovascular imaging agents/techniques

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**Introduction**

Fractional flow reserve (FFR) is defined as the ratio of the mean distal coronary pressure (Pd) measured with a pressure wire to the mean proximal coronary pressure (Pa) measured at the guide catheter during maximum hyperaemic flow, usually achieved after bolus infusion of a pharmacological agent such as adenosine. The accuracy of FFR as an index of myocardial ischemia is validated and widely accepted.1–4 FFR-guided PCI improves patient outcomes, reduces number of stent insertions and lowers cost of treatment.1 However, it is used in <10% of PCI procedures even in the UK5 and less than 40% in European countries where the leaders in 2015 were Denmark (31%) and Belgium (29%),6,7 likely in part due to the additional time and cost incurred in performing invasive FFR.

Virtual FFR represents a novel, non-invasive method to assess FFR of a coronary artery lesion without the practical difficulties that limit the invasive technique. Recently, several virtual FFR methods have used full 3D segmentation and 3D computational fluid dynamics simulations. These take time, entail significant cost and require expertise in image-based computational fluid dynamics (CFD) coupled with either CT coronary angiograms or invasive rotational coronary angiography to calculate FFR without insertion of a pressure wire or use of pharmacological agents.8–12 With a view to reducing some of the above constraints, several groups are exploring simpler ‘reduced-order’ virtual FFR methods that involve 1D simulations, but still use a 3D segmentation to generate the 1D geometry.10,11

The aim of this study is to investigate whether useful virtual FFR results can be obtained with a 1D model using only a few basic measurements of stenosis geometry obtained from routine coronary angiographic images. This will enable fast, low cost and viable results for immediate decision-making in the clinic or catheter laboratory without complex image segmentation or complex CFD software.

**Methods**

**Study population**

In this single centre retrospective study, we included subjects aged ≥18 years who were investigated for chest pain with coronary angiography, and in whom a coronary stenosis was detected and were subsequently investigated with an FFR measurement after obtaining informed consent. Patients with in-stent restenosis at the target vessel, previous bypass surgery, and diffuse coronary disease were excluded.

**Coronary angiography and invasive FFR measurements**

Diagnostic coronary angiography was performed using a 5 F or 6 F catheter according to local procedures. At least 2 orthogonal projections were acquired of all potential coronary stenosis. After heparin (70–100 IU/kg IV) administration, and intra-coronary nitrate to obtain maximum coronary vasodilatation a calibrated 0.014-inch “PressureWire” guide wire (St Jude Medical, USA) was introduced into the guiding catheter. The pressure wire was advanced into the guiding catheter until the pressure transducer was just outside its tip, and the pressure measured by the sensor was then normalized to that of the guiding catheter. The wire was then advanced into the vessel, distal to the target coronary stenosis. FFR was calculated as the lowest ratio of distal coronary pressure divided by aortic pressure after achievement of maximal hyperaemia at the steady-state, obtained using adenosine administration. Maximal hyperaemia was assumed after at least 1 minute in the presence of stable systemic blood pressure, decreased compared with baseline, remaining for at least 10 beats.13

**Quantitative coronary angiography**

Quantitative assessment of stenosis severity at coronary angiography was performed offline and independently by two cardiologists using two-dimensional Quantitative Coronary Angiography (QCA) with a computer assisted automatic arterial contour detection system (Centricity CA-1000, GE Healthcare, Little Chalfont, United Kingdom) in the end-diastolic angiographic image, with optimal projection showing minimal foreshortening of the lesion. The software utilizes measurement calibration by comparing it with an object of known dimension and allows rapid quantification of vessel size and lesion length.

The cardiologists were blinded to clinical and hemodynamic data. Pixel size was determined with automated distance calibration and all analyses were performed on frames demonstrating optimal luminal opacification. The proximal and distal limits of the lesion were defined by manual inspection (corresponding to the sites of minimal luminal encroachment i.e., mean 10% diameter decrease compared with the reference vessel). The automated edge-detection software was then used to trace the lesion contours and determined the reference vessel diameter and luminal diameter at maximal obstruction. Reference vessel diameter (RVD), lesion length (LL), minimal lumen diameter (MLD), and percentage diameter stenosis (DS) were calculated.
Calculation of 1D FFR: Patient specific data to calculate an estimate of flow rate

For all patients height and weight were recorded and a value of body surface area (BSA) calculated.\textsuperscript{14} To avoid the need for additional invasive measurements a number of assumptions were applied. From the BSA, cardiac output was approximated based on an assumed cardiac index of 3 L/min/m\textsuperscript{2}, derived from healthy subjects >60 years old using cardiac magnetic resonance imaging.\textsuperscript{15} A coronary flow reserve of 3 was assumed, based on data in human subjects presenting with chest pain and who had angiographically normal coronary arteries.\textsuperscript{16} Based on the estimated cardiac output, estimated total coronary blood flow was derived from an assumed myocardial mass based on the relationship between normalized proximal arterial diameters and myocardial mass for different segments of LAD, LCX and RCA.\textsuperscript{17} Vessel-specific baseline coronary flow was then assumed to be proportional to subtended myocardial mass, based on an allometric scaling principle.\textsuperscript{17–21} Cross-sectional areas of LCA and RCA were calculated from LCA and RCA measurements, then allometric scaling was carried out by initially calculating flow through the left main coronary artery, assuming flow is divided between LCA and RCA in proportion to their areas. The coronary flow in the stenotic branch was calculated based on the area ratio of the stenotic branch to the left main coronary artery. An estimate of the hyperaemic flow was then derived from which a mean flow rate in the vessel of interest was obtained. We assumed that the increase in flow under hyperaemic conditions is proportional to the resting flow, by reducing coronary resistance by a factor of 0.22, corresponding to a 3.5-fold increase in flow with respect to resting conditions.\textsuperscript{22} The performance of these modelling assumptions was further tested by re-analysing all results using other possible parameters but none achieved a better diagnostic accuracy (supplementary material).

1D Computational flow analysis

The coronary geometrical data was extracted offline from 2-dimensional coronary angiograms using QCA. The extracted data (Reference vessel diameter (RVD), lesion length (LL), minimal lumen diameter (MLD), and percentage diameter stenosis (DS)) was then combined with the estimated patient specific coronary flow rate calculated above and was incorporated into the 1D model containing wave speeds, material properties of the arteries and boundary conditions. Our code then generates the mesh to be introduced for analysis.\textsuperscript{23} This creates estimates of pressure (PD and PA) from which 1D-vFFR can be derived (Figure 1). The model uses established methods described extensively previously.\textsuperscript{23–25}

A coronary artery is represented as single segment, split into three parts, proximal part, stenosis and distal part is represented individually as one-dimensional (1D) segments, described by the equations of fluid flow and an equation governing the non-linear pressure-area elasticity relation. The coronary stenosis was represented with the lumped parameter stenosis model described by Young and Tsai,\textsuperscript{26} which contains empirically validated coefficients derived from stenosis length and relative diameter. Based on preliminary studies, the main determinant of FFR in such models is the flow through the stenosis. A representative coronary flow waveform was prescribed at the inlet, while the patient-specific mean flow passing through the stenosis was estimated as described above.

Statistical analysis

Statistical analysis was performed using the Statistical Package for the Social Sciences (SPSS 23.0, IBM Corp., Armonk, New York, USA). The correlation (Pearson) of both 1D-vFFR and QCA were compared to FFR. The diagnostic accuracy of 1D-vFFR was compared with QCA and against pressure-derived FFR using point estimates of sensitivity and specificity, and area under the curve analysis from receiver-operator characteristic curves (ROC). Statistical significance was accepted at a value of $p < 0.05$.

Results

The 85 patients included 62 males with mean age of 64 ± 9 years old. Baseline characteristics of all patients are shown in Table 1. Mean FFR was 0.84 (SD 0.07) and 32% of the stenoses had an FFR value <0.80, and hence underwent revascularization. QCA revealed the mean percentage of coronary stenosis by area was 54% ± 16% and the mean lesion length 13 ± 7 mm. Once angiographic images of the coronary artery had been acquired calculation of the 1D-vFFR took less than 1 minute. Coronary stenosis (QCA) had a statistically significant but weak
correlation with FFR ($r = -0.2$, $p = 0.04$) and poor diagnostic performance to determine lesions causing significant reductions in FFR ($< 0.80$), (area under the receiver operator characteristic curve (AUC) 0.39, $p = 0.09$). If a QCA area stenosis of 50% was taken as the cut off the sensitivity to detect a significant stenosis (FFR $< 0.8$) was 58% and the specificity 26%. If a more severe QCA area stenosis of 70% is used, then the sensitivity decreases to 11% with an increase in specificity to 71%. Compared with QCA, 1D-vFFR had a stronger correlation with FFR ($r = 0.32$, $p = 0.01$). Although the correlation between 1D-vFFR and FFR was only modest, 1D-vFFR provided an improvement in diagnostic accuracy over QCA (Figure 2). Overall compared with QCA, it showed significantly better diagnostic performance (AUC 0.67, $p = 0.007$) (Figure 3). Using a 1D-vFFR cut of 0.7 gave a sensitivity of 92% and a specificity of 29%.

**Discussion**

**QCA vs. 1D-vFFR**

We found that QCA was poor at determining a functionally significant stenosis by FFR. A QCA stenosis cutoff of 50% had a sensitivity of only 58% to detect an FFR $< 0.80$, in contrast, if 1D-vFFR was used with a cut off 0.75 then the sensitivity was 83%. If the more stringent 1D-vFFR cut off 0.70 is used, then the sensitivity goes up to 92%, specificity is 29%.

**Computational based methods to derive FFR**

Calculation of FFR derived from CTCA has been performed for some time using 3D models of the coronary tree and ventricular myocardium modelled from a mid-diastolic time point. The coronary tree is segmented into millions of separate finite elements and

**Table 1.** Baseline characteristics of all patients ($n = 85$).

| Mean age, years | 64(9) |
|-----------------|-------|
| Male, n         | 62    |
| BMI, kg/m²      | 28.3(4) |
| Coronary arteries, n |
| RCA             | 19    |
| PDA             | 1     |
| LMS             | 1     |
| LAD             | 67    |
| LCX             | 11    |
| D1              | 1     |
| OM1             | 2     |
| QCA Mean coronary stenosis area, % | 54 (16) |
| Coronary stenosis diameter/mm | 1.31(0.5) |
| QCA Mean coronary stenosis diameter, % | 44(12) |
| QCA Mean lesion length, mm | 13 (7) |

BMI: body mass index, RCA: right coronary artery, PDA: posterior descending artery, LMS: left main stem, LAD: left anterior descending, LCX: left circumflex artery, D1: first diagonal branch, OM1: first obtuse marginal branch, QCA: quantitative coronary angiography.

**Figure 2.** (a) Positive stenosis by QCA ($> 70\%$) correctly predicts positive FFR ($< 0.80$) with 1D-vFFR also positive ($< 0.75$). (b) Positive stenosis by QCA ($> 70\%$) provides a false positive reading as FFR is $> 0.80$, 1D-vFFR ($> 0.75$) correctly predicts lesion in not functionally significant.

**Figure 3.** Receiver operator characteristics (ROC) Curves comparing the diagnostic utility of mean area stenosis (derived from Quantitative Coronary Analysis (QCA)) and 1D-vFFR.
computational flow dynamics used to calculate the pressure loss at specific locations by solving the Navier-Stokes equations. However this is computationally very demanding requiring export of the images to a specialist facility with a processing time of at least 24 hours. This derived $\text{FFR}_{\text{CT}}$ (HeartFlowInc, California, US) had a sensitivity of 85% and specificity of 79% in intermediate (30%–70%) stenosis.3 If used as a “gatekeeper” pre catheter lab it has been shown to reduce the number of coronary angiograms showing non-significant disease without impacting on the number requiring PCI.27 $\text{FFR}_{\text{CT}}$ does have some limitations; numerous artefacts may affect CTA interpretability including calcification, misalignment, motion, and increased image noise. These may affect the model accuracy, preventing the calculation of an $\text{FFR}_{\text{CT}}$ in a third of cases in one study.28,29

**Angiography based methods to derive FFR**

Invasive angiography remains the most widely used modality to assess coronary anatomy and numerous methods have been used to attempt to derive a “virtual” FFR from the invasive angiogram. Morris et al. described one technique that derives the CT 3D coronary model from angiography rather than CTCA.30 This initially included pulsatile coronary flow which complicates the computation further requiring more than 24 hours to complete, however a later iteration utilising a “pseudo-transient” model of coronary flow reduced this time to <4 minutes but currently requires invasively measured coronary microvascular resistance.30 Both these techniques require rotational angiography which is not widely available and reduces their applicability. Other models use 3D-QCA and simplified computational flow modelling to rapidly derive a virtual FFR.31,32 The latter, QFFR was recently evaluated in the prospective, multi-centre FAVOR II trial where it demonstrated a sensitivity of 87% to detect invasive measured FFR positive lesions.31 Although promising, the requirement for 3D QCA, a modality not widely available limits its current utility.

**Potential of reduced order models**

Reduced order models for coronary haemodynamics are attractive as they are very quick and can easily incorporate relevant anatomical information. A reduced-order model is used to calculate the pressure and flow distribution for each coronary tree.

Subsequently, for each location along the coronary tree, we extract quantitative features describing the anatomy as well as the computed FFR value at that location. They have existed since the 1970s with Young and Tsai26,32 able to predict pressure drops within about 20% for a variety of flow conditions and stenosis geometries, including both symmetric and nonsymmetric stenosis. Pellicano et al. describe $\text{FFR}_{\text{angio}}$ which utilises a hybrid reduced order formulation with reduced order modelling of coronary flow in healthy regions and a more complex model in coronary stenosis.33 In the recent FAST-FFR trial this demonstrated impressive sensitivity (94%) to detect invasive FFR measured coronary stenosis.34 The model only requires standard angiographic images and the computational processing time is less than 3 minutes, however, image segmentation is still required which is done by specialised software which is then manually corrected, for which the time required is not specified and accounted for as a limitation.34

In this study we used a 1D model initially described by Mynard and Nithiarasu.25 Application of 1D models to coronary circulation have shown promising results using CTCA25,34,35 but to date this study is first to determine FFR from a standard coronary angiogram using a purely 1D model without 3D segmentation.

**Limitations**

Several limitations should be acknowledged. Our results represent a retrospective, small single centre experience including 102 intermediate coronary stenoses only and hence needs confirmation with larger, prospective multi-centre studies. In addition, patients who had previously undergone revascularization via coronary artery bypass grafting (CABG) surgery or had re-stenosis lesions were excluded from the study; for that reason, the accuracy of 1DFFR in these populations remains unknown.

Although at a cut off of 0.75, 1D-vFFR achieved a good sensitivity (83%), good positive predictive value (74.7%) and accuracy (68.6%) it had a low negative predictive value (52.4%) and specificity (35%) which meant a high rate of false positive (64.5%). With a cut off of 0.70, 1D-vFFR showed a higher sensitivity (92%), comparable positive predictive value (74.1%), better accuracy (72%) and negative predictive value (60%), but lower specificity (29%) and higher false positives (71%). This is most likely due to the assumptions that are inevitably required for the approach that we adopted; for example, improved estimation of hyperaemic coronary blood flow may improve accuracy further. In addition, stenosis geometry was represented by only three parameters (reference vessel diameter, percent stenosis and stenosis length); although missing complex features of the geometry, this approach was intentionally adopted to avoid the complex and time-consuming 3D segmentation process.
Conclusion

1D-vFFR improves the determination of the functional significance of coronary lesions compared with conventional angiography. It is derived using routine angiographic data and does not require a pressure-wire or hyperaemia induction. Standard QCA is used and no specialised image segmentation is required meaning it is fast enough to influence immediate clinical decision making and simple enough to be easily incorporated in the clinical workflow. Whilst the high sensitivity achieved raises the possibility that positive invasive FFR may be predicted in patients with a low 1D-vFFR, future work is required to establish whether this approach could have clinical value.

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Contributorship

JPM, PN and DRO developed the idea and designed the study. KM, GD and RD participated in data collection. KM and JPM analyzed the data. KM generated the first draft of the paper. JPM and DRO reviewed the draft and amended it. All authors approved the final version.

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Supplemental material

Supplemental material for this article is available online.

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