PHOTOMETRY AND THE BLAZHKO EFFECT IN THE RR Lyr VARIABLE STAR Y Vul

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ABSTRACT. The RR Lyr variable star Y Vul have been observed by using a CCD photometer during several seasons from 2011 to 2017. Nearly 5960 datapoints were obtained spanning over 53 nights. We found the amplitude and phase modulations with the amplitudes of 0.16 mag and 0.041 of the pulsating phase in V filter; 0.15 mag and 0.041 of the pulsating phase in R filter, respectively. The frequency Fourier analysis of the light curves with the help of Period04 software was performed, Blazhko modulation period (59.20 days) and triplet structures in the Fourier spectrum were detected. The pulsation frequency components in the Fourier spectrum were identified up to the 7th harmonic order, while the modulation side lobe frequencies – up to 9th order. The analysis of the light curves maxima resulted in the same value of the Blazhko period. The fundamental pulsation period of the star has been practically stable over a period of a hundred years.

Keywords: Stars: variables: RR Lyr stars – Y Vul.

1. Introduction

Y Vul (AN 1907.0004, Gaia DR1 - 286.0678990585, USNO-A2.0 1125 - 11247385), \( (\alpha^J_{2000} = 19^h 04^m 16.3^s; \delta^J_{2000} = +24^\circ 47' 19.1'' ) \) is known as the variable star for more than hundred years, but this RRab variable has been poorly investigated. The variability of the star was explored by van Biesbroeck and Casteels (1914), and they have defined that the star belongs to RR Lyr variables. However, in spite of their detailed observations, the authors haven’t deduced the light curve elements. Using observation data, reported by van Biesbroeck and Casteels, Tsevsevich (1960) derived a period and epoch of Y Vul as follows:

\[ MaxJD = 2419221.531 + 0^d.44941 \times E. \]  

He pointed out the difference in height of the light curves maxima and suspected the presence of the Blazhko effect in Y Vul. Using photographic observations in the range JD 2433034-41492, Kazarovets and Shugarov (1973) determined elements of the light-curve variation more accurately:

\[ MaxJD = 2438939.413 + 0^d.44945164 \times E. \]  

Their estimated range of the light variation was 14".2 - 16".0 (pg). The data reported in their study for Y Vul were included to the General Catalogue of Variable Stars (GCVS) (Samus’ at al. 2017) and AAVSO Variable Star Index (VSX database, https://www.aavso.org/vsx/index.php).

2. Observations

The photometric CCD observations of Y Vul were obtained at the Astronomical station near Odesa during the observation seasons in 2011-12, 2014-16 years in V filter; later on, in 2017 year the observations were performed in R filter using the 48 cm reflector AZT-3 of Astronomical observatory of Odesa National University, equipped with CCD photometer and Peltier cooler.
Table 1: The magnitudes of the comparison and check stars (NOMAD).

| Star   | $\alpha$, $\delta$ 2000 | magB   | magV   | magR   |
|--------|------------------------|--------|--------|--------|
| comA   | 19 04 12 -12.14.63     | 13.76  | 13.09  |
| comB   | 19 04 08 -12.905       | 12.424 | 12.090 |
| check  | 19 04 15 -14.40        | -      | 14.18  |
| Y Vul  | 19 04 16 -15.180       | 14.680 | 15.070 |

The datasets consists of 4290 V-band data points and 1665 Rc-band points obtained from over 53 nights of observations. Two stars were chosen as comparison and one as check stars as close as possible in B-V color. The magnitude of comparison star comB we have took from NOMAD catalogue (NOMAD 2005). We accepted these magnitudes and measured star comA relative to star comB on our frames. The resulting magnitudes for star comA are: V = 13.76, R = 13.09 with errors of 0.02 mag. The exposure time for variable and comparison stars was chosen to except a saturation of the frame and appointed as 120 sec. The BVR magnitudes of the variable, comparison and check stars from NOMAD catalogue; are summarized in Table 2.

The standard reduction of the CCD frames were carried out by using the MUNIPACK (Motl, http://sourceforge.net/projects/e-munipack ) software. The procedures for an aperture photometry is composed of the dark-level and flat-field corrections, determination of the instrumental magnitudes and precision. The magnitude of comparison star "com A" was used to convert the differential magnitudes to the corresponding value of variable. The photometry was transformed to the standard VRc Johnson-Cousins system by means of the differential photometry method (Benson 1998). The transformation coefficient was determined from observations of standard stars (Udovichenko 2012). The finding chart with market-out variable, comparison and check stars is shown in Fig. 1, the whole dataset of observations is presented in Fig. 2. The errors in individual data points vary from 0.005 to 0.02.

3. Frequency spectrum analysis

All data on the light variation curves nearby maxima and minima have been approximated by polynomials of 2-7 degrees with the best fit option by using software MCV (Andronov and Baklanov 1998). Then amplitudes of light variations and times of maxima have been defined. The observations of Y Vul shows the whole amplitude variation 1.05 in Rc-band and 1.33 in V-band. The modulation occurs at the maximum brightness and phase shift too. The brightness at maxima of the light curves in Rc-band vary from 14.265 to 14.411, the moderate Blazhko modulation of the amplitude reaches about 0.146; in V-band vary from 14.316 to 14.478, and the modulation reaches 0.162. The phase shift modulation in both bands varies within about 0.041 of the pulsation phase. All light curves of the target star obtained by using V and Rc filters with the pulsating period, are shown on Fig. 3. These phase curves were computed by using GCVS elements, equation 2.

To analyse the modulation properties of the light curves for this star, we have used a common technique a Fourier decomposition. The frequency analysis was performed using a package of computer programs with sine-wave fitting by using utilize Fourier algorithms (program Period04), (Lenz and Breger 2005). To capture longer time interval, we calculated observations, obtained with V-band and Rc-band.

The fundamental pulsation period was determined with the help of using the above-mentioned techniques as the highest peak on the Fourier amplitude spectrum. The observed harmonics and triplet were defined by pre-whitening data and Fourier analysis of the residuals. For each calculated harmonic and triplet, the signal-to-noise ratio has been estimated to retain only
significant signals greater than 4. The amplitude and phase for each frequencies, obtained with the best fitting, are given in Table 2.

The amplitude spectrum for the basic pulsating frequency and after pre-whitening are shown in Fig. 4. The harmonics of \( f_0 \) are significant to the 7th order, triplets \( f_0 \pm f_m \) to 9th order. The fundamental pulsating period \( P_0 = 0.44945177 \) is very close to the GCVS value. The Blazhko frequency also was determined as the difference of frequencies \( f_m = k f_0 - k f_0 \pm f_m \) and given in the last column of Table 2. Some of these frequencies contains an alias frequencies \( \sim (1/365 = 0.0027) \) as a result of the several seasons of observations (2011-17). Keeping that in mind we only used non-aliased frequencies to determine the Blazhko frequency. The average value equals \( 0.01689 \pm 0.0004 \) cd\(^{-1}\), whith corresponds to the period of \( 59.20 \pm 0.14 \) day.

The amplitude asymmetry is observed in the modulation components:

\[
Q_i = \frac{(A_{i+1}^+ - A_{i-1}^-)/(A_{i+1}^+ + A_{i-1}^-)}{(A_{i+1}^- + A_{i-1}^+)}
\]

where \( A_{i+1}^+ = f_0 + f_m \), \( A_{i-1}^- = f_0 - f_m \). The asymmetry ratios for the first component \( Q_1 = 0.36 \); the triplet ratios in the side lobes \( R_1 = A_{i+1}^- / A_{i-1}^+ = 2.16 \). The amplitudes of the pulsation components which decrease with increasing orders are smooth while the amplitudes of the modulation components decrease irregularly.

4. Light curves maxima analysis

The times of maxima in the all light curves was performed with help of fitting the light curve near the maxima by a polynomial function an order from 2 to 7. The list of observed light curves maxima presents in Table 3. The modulation Blazhko period was determined by the (O-C) period analysis (using Period04). The both method (i.e. frequency spectrum analysis and (O-C) deviation at maximum) have shown the same value of a Blazhko period. The value from the light curves maxima analysis equal \( 59.20 \pm 0.02 \) days. We selected the highest observed maximum and derived the elements of the Blazhko cycle:

\[
MaxHJD_{Blazhko} = 2457548.505 + 59.20 \times E_{Blazhko}
\]

The O-C diagram of Y Vul versus the Blazhko phase with sinusoidal fitting curve is presented in Fig. 5 (top). The O-C values are different in 9% of the pulsation period, the magnitudes at maximum are different in 12-14% of the V and Rc amplitude.

The O-C diagram was constructed by using all the published observational data available (Tsessevich 1960; Kazarovets and Shugarov 1973) as well as the data, obtained in this study by using the GCVS elements. The resulting diagram with linear fit is plotted in Fig. 5 (bottom). The data covers the
Table 2: Identify frequencies, amplitudes, phases and modulation frequencies $f_m = k f_0 - k f_0 \pm f_m$ of the V and Rc light curve solutions of Y Vul.

| Identification | $f$ (cd$^{-1}$) | amplitude, mag | phase, rad/2$\pi$ | snr | $f_m$ (cd$^{-1}$) |
|----------------|----------------|----------------|-------------------|-----|-----------------|
| $f_0$          | 2.224936(2)    | 0.311(1)       | 0.084(1)          | 94.2|                 |
| $2f_0$         | 4.449874(3)    | 0.187(2)       | 0.303(2)          | 35.2|                 |
| $3f_0$         | 6.674817(3)    | 0.160(1)       | 0.845(2)          | 31.4|                 |
| $4f_0$         | 8.899735(3)    | 0.100(2)       | 0.203(3)          | 22.1|                 |
| $5f_0$         | 11.12464(1)    | 0.050(4)       | 0.63(1)           | 13.5|                 |
| $7f_0$         | 15.5717(6)     | 0.029(8)       | 0.06(2)           | 9.2 |                 |
| $f_0+f_m$      | 2.24188(3)     | 0.031(9)       | 0.07(1)           | 7.1 | 0.01694(3)      |
| $f_0-f_m$      | 2.20803(6)     | 0.027(8)       | 0.3(3)            | 6.7 | 0.01691(6)      |
| $2f_0-f_m$     | 4.433004(9)    | 0.051(2)       | 0.268(7)          | 5.6 | 0.01687(1)      |
| $3f_0+f_m$     | 6.691688(7)    | 0.046(2)       | 0.088(6)          | 9.3 | 0.01688(1)      |
| $4f_0-f_m$     | 8.91661(1)     | 0.040(2)       | 0.952(9)          | 9.5 | 0.01687(1)      |
| $6f_0-f_m$     | 13.33284(5)    | 0.038(9)       | 0.069(3)          | 11.4| 0.01678(5)      |
| $7f_0+f_m$     | 15.59158(2)    | 0.018(3)       | 0.71(3)           | 4.5 | 0.01702(2)      |
| $8f_0-f_m$     | 17.78265(1)    | 0.017(2)       | 0.71(2)           | 4.0 | 0.01684(1)      |
| $9f_0+f_m$     | 20.06767(1)    | 0.09(1)        | 0.7(3)            | 7.2 | 0.0168(1)       |

| Identification | $f$ (cd$^{-1}$) | amplitude, mag | phase, rad/2$\pi$ | snr | $f_m$ (cd$^{-1}$) |
|----------------|----------------|----------------|-------------------|-----|-----------------|
| $f_0$          | 2.22491(6)     | 0.432(4)       | 0.992(2)          | 56.2|                 |
| $2f_0$         | 4.4497(1)      | 0.152(3)       | 0.715(8)          | 36.6|                 |
| $3f_0$         | 6.6744(4)      | 0.105(2)       | 0.415(4)          | 27.5|                 |
| $4f_0$         | 8.8994(4)      | 0.073(4)       | 0.813(8)          | 16.2|                 |
| $5f_0$         | 11.1235(7)     | 0.043(6)       | 0.62(2)           | 13.0|                 |
| $6f_0$         | 13.50(6)       | 0.022(8)       | 0.9(3)            | 5.0 |                 |
| $7f_0$         | 15.5757(1)     | 0.021(3)       | 0.19(1)           | 5.0 |                 |
| $f_0-f_m$      | 2.2094(3)      | 0.038(4)       | 0.17(1)           | 6.9 | 0.0151(3)       |
| $2f_0+f_m$     | 4.465(4)       | 0.035(9)       | 0.9(3)            | 8.4 | 0.0154(4)       |
| $3f_0-f_m$     | 6.659(2)       | 0.037(8)       | 0.7(1)            | 9.6 | 0.016(2)        |
| $4f_0+f_m$     | 8.916(4)       | 0.038(3)       | 0.30(1)           | 8.4 | 0.016(4)        |
| $5f_0-f_m$     | 11.109(2)      | 0.028(9)       | 0.6(1)            | 8.3 | 0.016(2)        |
| $8f_0-f_m$     | 17.782(4)      | 0.016(3)       | 0.4(1)            | 4.6 | 0.017(4)        |

period of a hundred years. The O-C difference over such long period less than 0.02 day, which is less than the Blazhko phase change. It allows to assume, that Y Vul has practically no secular period changes. The scattering of dots is due to the Blazhko effect.

5. Conclusions

This paper describes the modulation of the light curves of a RR Lyrae variable Y Vul. Using the data obtained from the several observational seasons, we have found the Blazhko effect for the pulsating in the fundamental mode. The amplitude of the maximum brightness variation reaches $0^m.162$ with V filter and $0^m.146$ in Rc filter; the phase shift is 0.041 of pulsation phase. Using the Fourier analysis for these data we have derived the fundamental pulsating period of $0.4494517 \pm 0.000001$ day. The Blazhko period was defined using the O-C value at maxima and frequency spectrum analysis. The average period equal 59.20 $\pm$ 0.02 days. The modulation of the Y Vul light curves are described by the triplet frequencies $k f_0 \pm f_m$ and the modulation frequency $f_m$. In the frequency spectrum

Figure 5: The O-C (day) diagram of Y Vul versus Blazhko phase with the sinusoidal fitting curve (top figure). The O-C (day) diagram of Y Vul during over a hundred years with the linear fitting (bottom figure).
| Maximum HJD | Error | Magnitude (V-C) | Error | Cycle | O - C | Phase | Error | Filter |
|------------|-------|-----------------|-------|-------|-------|-------|-------|-------|
| 2455735.4040 | 0.00019 | 0.6209 | 0.0028 | 37569 | -0.0168 | -0.0374 | 0.0004 | V |
| 2455793.3841 | 0.00021 | 0.6288 | 0.0027 | 37516 | -0.0199 | -0.0444 | 0.0005 | V |
| 2455801.4702 | 0.00025 | 0.6315 | 0.0027 | 37518 | -0.0184 | -0.0410 | 0.0003 | V |
| 2455802.3706 | 0.00018 | 0.6315 | 0.0027 | 37518 | -0.0184 | -0.0410 | 0.0003 | V |
| 2455805.5187 | 0.00071 | 0.6752 | 0.0112 | 37525 | -0.0165 | -0.0367 | 0.0015 | V |
| 2455824.4119 | 0.00028 | 0.5622 | 0.0049 | 37567 | -0.0002 | -0.0006 | 0.0006 | V |
| 2455825.3101 | 0.00023 | 0.5534 | 0.0034 | 37569 | -0.0010 | -0.0022 | 0.0005 | V |
| 2456156.5371 | 0.00031 | 0.6479 | 0.0034 | 37516 | -0.0199 | -0.0444 | 0.0005 | V |
| 2456158.3380 | 0.00023 | 0.5622 | 0.0049 | 37567 | -0.0002 | -0.0006 | 0.0006 | V |
| 2456180.3773 | 0.00020 | 0.5633 | 0.0033 | 37569 | -0.0010 | -0.0022 | 0.0005 | V |
| 2456181.2759 | 0.00026 | 0.5690 | 0.0041 | 37569 | -0.0009 | -0.0021 | 0.0005 | V |
| 2456207.3276 | 0.00048 | 0.6349 | 0.0055 | 38419 | -0.0174 | -0.0387 | 0.0010 | V |
| 2456208.2265 | 0.00024 | 0.6276 | 0.0021 | 38421 | -0.0174 | -0.0387 | 0.0005 | V |
| 2456208.3714 | 0.00022 | 0.6290 | 0.0029 | 38421 | -0.0174 | -0.0387 | 0.0005 | V |
| 2457548.5045 | 0.00027 | 0.5528 | 0.0048 | 41403 | -0.0041 | -0.0092 | 0.0006 | V |
| 2457593.4476 | 0.00031 | 0.5661 | 0.0040 | 41503 | -0.0063 | -0.0140 | 0.0007 | V |
| 2457594.3460 | 0.00030 | 0.5609 | 0.0050 | 41505 | -0.0067 | -0.0150 | 0.0006 | V |
| 2457606.4806 | 0.00022 | 0.5664 | 0.0027 | 41532 | -0.0073 | -0.0163 | 0.0004 | V |
| 2457657.2674 | 0.00028 | 0.5710 | 0.0045 | 41645 | -0.0066 | -0.0147 | 0.0006 | V |
| 2457665.3550 | 0.00029 | 0.5695 | 0.0044 | 41663 | -0.0111 | -0.0248 | 0.0006 | V |
| 2457666.2574 | 0.00040 | 0.5599 | 0.0069 | 41665 | -0.0076 | -0.0169 | 0.0009 | V |
| 2457899.5228 | 0.00043 | 0.5565 | 0.0078 | 42184 | -0.0076 | -0.0170 | 0.0010 | V |
| 2457930.5197 | 0.00033 | 1.2740 | 0.0062 | 42253 | -0.0229 | -0.0509 | 0.0007 | R |
| 2457935.4185 | 0.00038 | 1.2249 | 0.0043 | 42255 | -0.0229 | -0.0510 | 0.0008 | R |
| 2457935.4719 | 0.00051 | 1.2772 | 0.0060 | 42264 | -0.0146 | -0.0325 | 0.0011 | R |
| 2457936.3699 | 0.00073 | 1.2708 | 0.0075 | 42266 | -0.0155 | -0.0345 | 0.0016 | R |
| 2457936.4967 | 0.00034 | 1.1902 | 0.0054 | 42304 | -0.0055 | -0.0124 | 0.0007 | R |
| 2457958.4014 | 0.00070 | 1.1700 | 0.0064 | 42315 | -0.0071 | -0.0159 | 0.0015 | R |
| 2457966.4924 | 0.00036 | 1.1909 | 0.0074 | 42333 | -0.0063 | -0.0141 | 0.0008 | R |
| 2457993.4484 | 0.00066 | 1.2576 | 0.0089 | 42393 | -0.0174 | -0.0388 | 0.0014 | R |

The pulsation harmonic components are detected up to the 7th order; the modulation side lobe frequencies are detected up to 9th order. Thirty pulsation maxima from the observed light curves have been measured. The fundamental pulsation period of the star has been practically stable over a period of a hundred years.

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