Investigating Taxonomic Diversity within Asteroid Families through ATLAS Dual-band Photometry

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Abstract

We present here the c–o colors for identified Flora, Vesta, Nysa–Polana, Themis, and Koronis family members within the historic data set (2015–2018) of the Asteroid Terrestrial-impact Last Alert System (ATLAS). The Themis and Koronis families are known to be relatively pure C- and S-type Bus-DeMeo taxonomic families, respectively, and the extracted color data from the ATLAS broadband c- and o-filters of these two families are used to demonstrate that the ATLAS c–o color is a sufficient parameter to distinguish between the C- and S-type taxonomies. The Vesta and Nysa–Polana families are known to display a mixture of taxonomies possibly due to Vesta’s differentiated parent body origin and Nysa–Polana actually consisting of two nested families with differing taxonomies. Our data show that the Flora family also displays a large degree of taxonomic mixing and the data reveal a substantial H-magnitude dependence on color. We propose and exclude several interpretations for the observed taxonomic mix. Additionally, we extract rotation periods of all of the targets reported here and find good agreement with targets that have previously reported periods.

Supporting material: figure set, machine-readable table

1. Introduction

Asteroid families are groups of objects where members of the group display similar proper orbital elements. This suggests a common collisionally disrupted parent-body source for a family. Since the identification of asteroid families (Hirayama 1918), several studies have also shown that for many of the identified families there is also a strong correlation between taxonomic type and family membership (Bus 1999). For instance, family members of the Massalia, Eunomia, and Koronis families all have observed spectra or colors that are consistent with the Bus-DeMeo S-type taxonomy (Lazzaro et al. 1999; Masiero et al. 2015; Erasmus et al. 2019). On the other hand, members of the Hygiea, Adeona, and Themis families all have observed spectra or colors that are consistent with the Bus-DeMeo C-type taxonomy (Carruba 2013; Masiero et al. 2015; Erasmus et al. 2019). This leads to the assumption that the individual parent-body sources of each of these families must have had a pure composition with either a S-type or C-type spectral signature (see Figure 1 for spectra in the visible of the Bus-DeMeo S- and C-type taxonomies).

However, there are several families that display a large variation in observed spectra or color and therefore potentially contain a significant mix of two (or more) taxonomies. Some explanations that have been proposed include: nested families, i.e., two overlapping families in orbital space that are actually two separate families with differing taxonomies (Cellino et al. 2001); two colliding parents that had completely different mineralogy; size-dependent space-weathering that modifies the spectral shape of a subgroup within the family (Brunetto & Strazzulla 2005); a large differentiated parent body having variations in mineralogy (Binzel & Xu 1993); or simply incorrectly assigning membership (sometimes referred to as interlopers).

In this work we present the c–o colors and rotation periods of 1612 (414 Vesta, 494 Flora, 304 Nysa–Polana, 204 Themis, and 197 Koronis) main-belt targets. In Sections 2 and 3 we briefly summarize the Asteroid Terrestrial-impact Last Alert System (ATLAS) system and the approach for identifying the relevant family members within its data set. In Section 4 we explain how the colors are derived from the data set’s dual-band photometry. The method for extracting color relies on the determination of the rotation periods, hence the latter are a convenient byproduct of our analysis. In Section 5 we discuss how we assign taxonomies to the targets. Section 6 contains results of validation tests using previously reported taxonomies and rotation periods. We also show validation results using the ATLAS c–o colors of the Themis and Koronis targets that have known and relatively pure taxonomic distributions. In Sections 7 and 8 we perform a more in-depth study on the observed taxonomic diversity of the Vesta, Nysa–Polana, and Flora families and use this to draw conclusions on the origin of the Flora family by comparing to the Vesta and Nysa–Polana families that have known reasons for the observed mixture in the taxonomies present.

2. ATLAS Data

Observations were performed between 2015 and 2018 by ATLAS. Currently consisting of two units both located in Hawaii, ATLAS is designed to achieve a high survey speed per
unit cost (Tonry et al. 2018a). Its main purpose is to discover asteroids with imminent impacts with Earth that are either regionally or globally threatening in nature. To fulfill this, the two current ATLAS units scan the complete visible northern sky every night enabling it to make numerous discoveries in multiple astronomical disciplines, such as supernovae candidate discovery (Prentice et al. 2018), gamma-ray burst phenomena (Stalder et al. 2017), variable stars (Heinze et al. 2018), and asteroid discovery. Since its inception ATLAS has found 39 potentially hazardous asteroids among the 370 near-Earth asteroids that it has discovered. All detected asteroid astrometry and photometry are posted to the Minor Planet Center, while the supernova candidates are publicly reported to the International Astronomical Union Transient Name Server.

The two ATLAS units are 0.5 m telescopes each covering 30 deg² field-of-view in a single exposure. The main survey mode mostly utilizes two custom filters, a “cyan” or C-filter with a bandpass between 420 and 650 nm and an “orange” or O-filter with a bandpass between 560 and 820 nm (see Figure 1). For further details on ATLAS, ATLAS photometry, and the ATLAS All-sky Stellar Reference Catalog see Tonry et al. (2018a, 2018b) and Heinze et al. (2018).

3. Family Determination

To identify Flora, Vesta, Nysa–Polana, Themis, and Koronis family members within the ATLAS data set we utilize and cross-correlate with data from Nesvorny (2015) obtained through The Planetary Data System (PDS) to associate objects from the ATLAS data set with known collisional families. The Nesvorny (2015) data set makes use of the Hierarchical Clustering Method (Zappala et al. 1990) to assign families. The data set also supplies a “c-parameter” (see Nesvorny 2015 for a description) that can be used to identify suspected interlopers. For the ATLAS data set the interloper contamination is low with a percentage of suspected interlopers for the Flora, Vesta, Nysa–Polana, Themis, and Koronis of 4.5%, 0.0%, 13.5%, 6.4%, and 5.6% respectively.

4. Rotation Period Extraction and Color Calculation

Rotation periods were extracted from the ATLAS data by generating a Lomb–Scargle periodogram (Lomb 1976; Scargle 1982) of each target’s O-filter photometric data since this is the most abundant data out of the two filters used by ATLAS. We only considered ATLAS targets that had at least 30 photometric data points in the O-filter and 10 photometric data points in the C-filter. See the top plots of Figure 2 for example O- and C-filter photometric data of Flora family member 1785 Wurm (1941 CD), Koronis family member 1809 Prometheus (2522 P-L), and Vesta family member 2511 Patterson (1980 LM). Targets that had periodograms containing peaks with a confidence (Zechmeister & Kürster 2009) larger than 50% were flagged to have potentially extractable rotation periods. See the middle plots of Figure 2 for example periodograms that resulted in high confidence peaks. The final extracted light-curve period is determined from the strongest periodogram peak, and the uncertainty of this periodicity is determined by fitting a Gaussian function to the periodogram peak and using the rms width (σ) as the uncertainty (see the superimposed black curve and σ of the fitted function in the periodogram plots in Figure 2). It has to be noted that because of the ATLAS observing cadence there is significant alias ambiguity in our periodograms due to the daily interval between observations. Therefore, there is the likelihood that some of the periods we extract are offset from the actual period by a frequency that is a multiple of a day (24 hr). This is evident by the presence of multiple peaks in some of our periodograms that have a similar confidence. The rotation periods (twice the extracted light-curve period), uncertainty, and confidence in the periods are recorded in Table 1.

To determine the colors of each ATLAS target we fold both the C- and O-filter data with the extracted rotation period. A spline fit in the form of a high-order polynomial is fitted to the more abundant O-filter data with the fit weighted on the uncertainty of the photometric values. The same polynomial that is fitted to the O-filter data, with the inclusion of a magnitude offset as a variable fit parameter, is fitted to the C-filter data. The C−O color is assigned as this fitted magnitude offset. The uncertainty in this color value is derived from the weighted (by uncertainty of the photometric values) standard deviation of the residuals of the two filter fits and the respective filter data. See the bottom plots of Figure 2 for examples of the results of this procedure with the C−O color values and uncertainty displayed in bottom left corner of each plot. This derived color value is not dramatically affected if by chance the folding is performed using an alias of the rotation period instead of the actual rotation period.

In a final step we remove photometric outliers and low-quality data from our data set by discarding targets that have a C−O color that falls more than 3σ from the median measured C−O color of the relevant family and targets that had an uncertainty in measured C−O color larger than 130% of the median uncertainty of the targets in the relevant family. The result was that we discarded on average roughly 25% of our targets for each family. The calculated C−O colors and the uncertainties are recorded in Table 1.

\footnote{https://pds.nasa.gov/}
Figure 2. Example ATLAS photometric data (top plots), Lomb-Scargle periodograms of photometric data (middle plots), and phased photometric data (bottom plots) for (a) Flora family member 1785 Wurm (1941 CD), (b) Koronis family member 1809 Prometheus (2522 P-L), and (c) Vesta family member 2511 Patterson (1980 LM). For the periodograms we also indicate the extracted light-curve period \( P_{\text{max}} \), uncertainty in extracted period \( \sigma \), and confidence in extracted period. Fitted to the phased data are spline fits in the form of a high-order polynomial which are used to determine the color of each target (see Section 4 for detail). The determined \( c-o \) color value and the uncertainty is displayed in the bottom-left of each plot. All 1612 images are available in the Figure Set. (The complete figure set (1612 images) is available.)

### Table 1

| No.  | Target Name       | Family       | \( H^a \) (mag) | \( c-o \) (mag) | Rotation Period (hr) | Confidence % | C-type (prob. in %) | S-type |
|------|-------------------|--------------|-----------------|-----------------|----------------------|--------------|--------------------|--------|
| 0001 | 158 Koronis       | Koronis      | 9.3             | 0.40 ± 0.09     | 14.204 ± 0.006       | 73           | 18                 | 82     |
| 0002 | 167 Urda          | Koronis      | 9.2             | 0.38 ± 0.06     | 13.060 ± 0.009       | 88           | 14                 | 86     |
| 0003 | 208 Lacrimosa     | Koronis      | 9.0             | 0.42 ± 0.09     | 14.087 ± 0.010       | 84           | 13                 | 87     |
| 0004 | 222 Lucia         | Themis       | 9.1             | 0.22 ± 0.09     | 9.371 ± 0.005        | 58           | 86                 | 14     |
| 0005 | 243 Idas          | Koronis      | 9.9             | 0.39 ± 0.10     | 4.225 ± 0.001        | 74           | 26                 | 74     |
| 0006 | 254 Augusta       | Flora        | 12.1            | 0.42 ± 0.12     | 5.895 ± 0.002        | 85           | 18                 | 82     |
| 0007 | 263 Dresda        | Koronis      | 10.2            | 0.39 ± 0.12     | 12.450 ± 0.055       | 72           | 28                 | 72     |
| 0008 | 277 Elvira        | Koronis      | 9.8             | 0.41 ± 0.04     | 29.676 ± 0.046       | 86           | 1                 | 99     |
| 0009 | 281 Lucretia      | Flora        | 12.0            | 0.44 ± 0.13     | 4.783 ± 0.001        | 70           | 17                 | 83     |
| 0010 | 352 Gisela (A893 AB) | Flora    | 10.0            | 0.43 ± 0.09     | 7.480 ± 0.003        | 82           | 10                 | 90     |

Note.

\( ^a \) \( H \) magnitude was obtained from https://ssd.jpl.nasa.gov/horizons.cgi.

(This table is available in its entirety in machine-readable form.)

5. Taxonomic Determination

For this study we limit our target classification to the two most prominent Bus-DeMeo taxonomic classes, namely, the silicate-rich S-type and the carbonaceous C-type that make up roughly 50% and 35% of the main-belt population, respectively (Bus & Binzel 2002; DeMeo & Carry 2014; Erasmus et al. 2018). Because the Bus-DeMeo S- and V-type spectra are difficult to distinguish using only two broadband filters in the visible region we consider those two both as S-type in this study. To decide which of these two classifications is the most likely for each of our targets we calculate the expected \( c-o \) ATLAS color for the mean Bus-DeMeo S- and C-type spectra provided by DeMeo et al. (2009) and compare that to the target’s measured \( c-o \) color. The expected \( c-o \) color is determined by convolving the ATLAS filter responses with the mean Bus-DeMeo S- and C-type spectra (see Figure 1 for filter responses and spectra) and use the convolution of the ATLAS filter responses with the Sun’s spectrum as the zero-point magnitudes. The same was done for the the upper and lower bounds of the spectra to determine the uncertainty in the expected color. The expected \( c-o \) color for an S-type asteroid is \( 0.388 \pm 0.011 \) and for a C-type is \( 0.249 \pm 0.004 \) (see the solid blue and red vertical lines in Figures 3–5 with the upper and lower bounds indicated in the dashed lines).

To assign the S- or C-type taxonomy to each of our targets we use a probabilistic approach using a Monte Carlo method where we generate 10,000 pseudo-measured colors with a
Figure 3. Plotted are the $c-o$ colors that could be extracted (see Section 4) from the ATLAS data set of (a) Themis family members and (b) Koronis family members. The data points are colored depending on the final assigned taxonomy (see Section 5, S-type = red and C-type = blue). The Themis and Koronis families are two known C- and S-type Bus-DeMeo taxonomic families, respectively, and the color histograms centered at the relevant mean Bus-DeMeo color therefore illustrate that the ATLAS $c-o$ color is a suitable parameter to distinguish between the C- and S-type taxonomies.

Figure 4. (Top) Plotted are the $c-o$ colors that could be extracted (see Section 4) from the ATLAS data set of (a) Vesta family members and (b) Nysa–Polana family members. The data points are colored depending on the final assigned taxonomy (see Section 5, S-type = red and C-type = blue). (Middle) Proper orbital elements of all ATLAS targets with all known family members from Nesvorny (2015) plotted as small black data points in the background (suspected interlopers plotted with a cross symbol). Also included are the histograms of the taxonomic probabilities (see Section 5) indicating the taxonomic dependence on orbital parameters. (Bottom) The cumulative probabilities of the two taxonomies with respect to the three orbital parameters: broad red line = S-type and narrow blue line = C-type (see Section 7).
normal distribution centered on the target’s measured color and the width of the distribution equal to the uncertainty in the measured color (see Navarro-Meza et al. 2019 for a similar approach using r-i colors to classify near-Earth asteroids). Each pseudo-measured color is classified as either S- or C-type depending on where it lies relative to the decision line located at the color value midway between the two expected c-o color values for an S- and C-type asteroid (i.e., c-o = 0.319; see the dotted black vertical line in Figures 3–5). The pseudo-measured classifications are tallied to give the S- and C-type taxonomic probabilities for each target. The taxonomy with the highest probability is assigned to the target (data points in Figures 3–5 are color-coded depending on the final assigned taxonomy, S-type = red and C-type = blue). We use the probabilities instead of the discrete classification for all our analyses in Sections 7 and 8. The taxonomic probabilities for each target are recorded in Table 1.

6. Validation of Rotation Periods and Taxonomic Determination

To validate our procedures of extracting rotation periods and determining taxonomic types, we cross-reference our results with The Asteroid Light Curve Database (LCDB; Warner et al. 2009, Updated 2019 January 31) and find that 10% of our targets are also present in the LCDB. For the 262 targets present in both data sets we derive the same taxonomy as that reported in the LCDB for 85% of the targets (for this we consider V-type and S-type as a match as well as B-type and C-type as a match) and also match the reported rotation periods within an error margin of 1% for 76% of our targets and within an error margin of 10% for 89% of our targets (for this comparison we also included the two alias periods adjacent to the main extracted period).

As a second validation test, the Themis and Koronis families, which are two well-known relatively pure C- and S-type Bus-DeMeo taxonomic families, are used as benchmarks for our taxonomic determination. In Figure 3 we plot the extracted c-o colors of the Themis and Koronis family members within the ATLAS data set. The data points are color-coded depending on the final assigned taxonomy, S-type = red and C-type = blue. Of the 204 Themis targets we classify 95% as C-type, and the color histogram shown in Figure 3(a) shows a clear peak centered at the expected mean Bus-DeMeo C-type color. Of the 197 Koronis targets we classify 91% as S-type, and the color histogram shown in Figure 3(b) shows a clear peak centered at the expected mean Bus-DeMeo S-type color. These two plots demonstrate that the ATLAS c-o colors that we extract are a sufficient parameter to distinguish between the C- and S-type taxonomies.

7. Mixture of Taxonomies in the Vesta and Nysa–Polana Families

The Vesta family, a V-type family, has a spectral signature similar to the spectral shape of S-type asteroids but with the distinct S-type absorption feature at 1 μm enhanced in V-types. The Nysa–Polana family is also a known S-type family. However, observations have indicated that both contain a significant number of family members with spectra or color different from the majority of family members (Erasmus et al. 2019). This could be ascribed to the parent body of the Vesta family originally consisting of a differentiated object (Russell et al. 2012) and hence a plausible reason behind the range in colors observed within the Vesta family. Through albedo studies the Nysa–Polana family has been identified to consist of two subgroups overlapping in proper orbital space (Cellino et al. 2001), i.e., two nested families of which one shows S-type spectral characteristics and the other B-type spectral characteristics. The Bus-DeMeo B-type spectrum is similar to the spectral shape of C-type asteroids, flat and featureless, but with a slightly bluer slope in the visible. The top set of plots in Figure 4 are the extracted c-o colors of the Vesta and Nysa–Polana family members within the ATLAS data set. The two-taxonomic mix is clearly evident in both families with only ~70% of Vesta targets having c-o colors in the vicinity of the expected S(V)-type color while the Nysa–Polana targets have a 1:3 split between c-o colors that match the expected C(B)-type and S-type colors, respectively.

9 http://www.MinorPlanet.info/lightcurvedatabase.html
By plotting the distributions of the two taxonomies as a function of proper orbital space (see the middle set of plots in Figure 4), the differing causes behind the taxonomic diversity seen in both of these families can be distinguished from one another. The assigned taxonomy of Vesta family members has no dependence on proper orbital space (consistent with a differentiated parent body origin), while the Nysa–Polana “B-type subgroup” is positioned at a lower eccentricity (and to a lesser extent a higher inclination) than the Nysa–Polana “S-type subgroup” (consistent with two nested families with slightly differing orbital parameters). This taxonomic dependence (or independence) on orbital parameters is highlighted by performing Kolmogorov–Smirnov (K-S) tests and plotting the resultant cumulative probabilities of the two taxonomies with respect to the three orbital parameters (see the bottom plots of Figure 4, broad red line = S-type and narrow blue line = C-type). The two taxonomies in the Vesta family have identical cumulative probabilities for the three orbital parameters (K-S statistics for semimajor axis, inclination, and eccentricity of 0.08, 0.04, and 0.01), while the two taxonomies in the Nysa–Polana family have obvious differing cumulative probabilities in eccentricity (K-S statistics for semimajor axis, inclination, and eccentricity of 0.05, 0.12, and 0.15). We use the cumulative probabilities of these two families as benchmarks for ascertaining the likely cause of the taxonomic diversity also seen in the Flora family.

8. Taxonomic Diversity of the Flora Family

The top plot in Figure 5 shows the the extracted c-o colors of the Flora family members within the ATLAS data set. As is the case with the Vesta and Nysa–Polana families, the Flora family also displays a significant taxonomic mix, or at least a significant range of colors. Roughly 70% of the targets have c-o colors consistent with the expected S-type color with the remaining targets displaying bluer C-like colors. This is a similar proportion to that of the Vesta family. The cumulative plots of the two colors in the Flora family (see the bottom of Figure 5) are identical for the three orbital parameters (as is the case for the Vesta family) as opposed to indicating a nested family as is the case for the Nysa–Polana family. Therefore, a nested family is unlikely as the source of the taxonomic mix in the Flora family.

9. Discussion

There are several possible interpretations for the taxonomic mix observed for the Flora family. Plotting the moving average of the colors as a function of H-magnitude (size) reveals a strong color dependence on size for the Flora family targets (see Figure 5). Since the smaller bodies are probably younger (more recently created through collisions) and therefore have fresher surfaces, one clear possibility is that the older surfaces on the larger bodies have been reddened through space weathering, whereas the younger surfaces on smaller bodies are unweathered and therefore less red. Thomas et al. (2011, 2012) report that small (H ≈ 15) Koronis family objects are bluer than large (H ≈ 12) Koronis family objects and attribute this difference to space weathering. We also observe a hint of this effect at a similar H-magnitude range in our Koronis family observations (see Figure 3(b)). However, this effect is subtle and cannot explain the large color range we observe for the Flora family (compare color ranges as a function of H-magnitude for the Koronis and Flora families in Figures 3(b) and 5).

Another possibility is that, like the Vesta family, the heterogeneous Flora family may show evidence of a differentiated parent body. This is in agreement with a differentiated-body speculation by Gaffey (1984) based on several mineralogic and petrologic parameters derived for the surface material of asteroid Flora. Spectral data from the Galileo spacecraft on its flyby of Flora-family member 951 Gaspra also showed an olivine/pyroxene ratio that points to Gaspra being a fragment of at least a partially differentiated parent body (Veverka et al. 1994). However, various work (Vernazza et al. 2008, 2014; Dunn et al. 2013) has shown that the Flora family is likely the source of the undifferentiated LL chondrites, making this interpretation potentially problematic.

Alternatively, the C-like asteroids in the Flora family may simply be interlopers in the family membership list, though this would imply a relatively high contamination fraction of 28.3% that is significantly higher than the estimate for our data set of only 4.5% using the model of Nesvorny (2015).

Finally, two additional possible causes for the C-like colors that are observed could be due to shocked material and impact melt, which Kohout et al. (2014) and Reddy et al. (2014) have shown can make LL chondrite (S-like) spectra appear more C-like, or that a large member of the original S-type Flora family was simply impacted by a C-type asteroid that shattered, producing an embedded family within the Flora family that has a separate parent body (here we define an embedded family as one that was created through a collision between a family member and a non-family member, whereas a nested family occupies similar orbital element space but has an independent origin). Neither of these interpretations can be excluded by the taxonomic independence on orbital parameters we observe. The strong color dependence on size of our observed Flora family targets can be explained if the C-type impactor was smaller (H ≈ 12) than the original S-type Flora parent body.

These topics are discussed in further detail in a forthcoming paper (H. Sun et al. 2020, in preparation).

10. Conclusion

We have reported the c-o colors (and rotation periods) for identified Flora, Vesta, Nysa–Polana, Themis, and Koronis family members within the historic data set (2015–2018) of ATLAS. By using a probabilistic approach we also classify our targets as either S-type or C-type and compare to previously reported taxonomies and rotation periods to validate our methodologies. We use the Themis (a C-type family) and Koronis (a S-type family) targets in the ATLAS data set to demonstrate that the ATLAS c-o color is a sufficient parameter to distinguish between the C- and S-type taxonomies.

We find that the Flora family has a significant mixture of red (S-like) and blue (C-like) colors and a compelling observed H-magnitude dependence on the colors and we propose several possible causes of this range in colors.

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