Scalar Mesons in B-decays

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Abstract. We summarize some persistent problems in scalar spectroscopy and discuss what could be learned here from charmless B-decays. Recent experimental results are discussed in comparison with theoretical expectations: a simple model based on penguin dominance leads to various symmetry relations in good agreement with recent data; a factorisation approach yields absolute predictions of rates. For more details, see [1].

WHY STUDYING SCALARS IN B-DECAYS

There are various reasons for studying scalar particles in B-decays:

1. Dominance of S-wave resonances with little background from crossed channels
   In \((B \rightarrow 1,2,3)\)-decays the masses of \((1,2)\) resonances can extend to \(M \lesssim 5\) GeV. Then there is little overlap with resonances in crossed channels \((2,3)\) or \((1,3)\). This is very different from \(D\) decays where resonance masses extend only up to \(\sim 1.5\) GeV and in general there is a large overlap. Furthermore, in the final 2-body systems S-wave interactions are dominant.

2. New source of glueballs
   The elementary subprocess \(b \rightarrow sg\) with an isolated gluon is rather well understood theoretically and is described by a penguin diagram. The decay rate has been calculated in next-to-leading order of perturbative QCD as \([2]\)
   \[
   B(b \rightarrow sg) = (5 \pm 1) \times 10^{-3}.
   \]
   The gluon may give rise to production of a glueball which could show up as a resonance in the system \(X\) of 2-body decays \(B \rightarrow K^{(*)} + X\). This process adds to the other well known gluon rich processes like: central production in \(pp\) collisions, \(J/\psi \rightarrow \gamma X\) and \(p\bar{p}\) annihilation near threshold.

3. Non-charm final states with strangeness
   The decays \(b \rightarrow sq\bar{q}\) are dominated again by the gluonic penguin process whereas the electroweak tree diagrams occur at the level of 20% only. In the leading penguin approximation the decays \(b \rightarrow su\bar{u}, sdd, ss\bar{s}\) occur with the same fraction and have been calculated to amount to \(\sim 2 \times 10^{-3}\) each. In the corresponding hadronic 2-body final states \(B \rightarrow xy\), if \(x\) and \(y\) are members of \(SU(3)\) multiplets \(X, Y\) each, one obtains various symmetry relations \([3]\). Hopefully, this will ultimately identify the members of the lightest scalar nonet and the mixing properties.
The interest in light scalar mesons originates from the following expectations:

1. **The existence of glueballs**
   This is a requirement from the first days of QCD and may be the most urgent open problem of the theory at the fundamental level. In lattice QCD, quenched approximation, the lightest glueball appears in the $0^{++}$ channel with a mass of 1400-1800 MeV \[4\]. The effect of unquenching is under study but realistic estimates are still difficult, especially because of the large quark masses. An alternative QCD approach is based on QCD sum rules \[5\] where the lightest glueball is centered around 1000-1400 MeV.

2. **Multiplets of $q\bar{q}$ and exotic bound states**
   There is no general consensus on the members of the lightest $q\bar{q}$ nonet, i.e. the parity partner of $\pi, K, \eta, \eta'$. In addition, there is the possibility of tetraquarks \[6\], bound states of di-quarks.
   The list of scalar particles provided by the PDG \[7\] with mass $M<\sim 1.8$ GeV includes
   \[ I=0: \ f_0(600) \ (or \ \sigma), \ f_0(980), \ f_0(1370), \ f_0(1500), \ f_0(1710); \]
   \[ I=\frac{1}{2}: \ \kappa(900) \ (?), \ K_0^*(1430); \]
   \[ I=\frac{3}{2}: \ \alpha(980), \ a_0(1450). \]
   There are two typical scenarios for the classification of these states:
   - **I. One nonet below and one above 1 GeV**
     The nonet of lower mass includes $\sigma, \kappa, f_0(980), a_0(980)$, either $q\bar{q}$ (see, for example, Ref. \[8\] and Van Beveren \[9\]) or $qq\bar{q}\bar{q}$ \[6\] bound states. The higher mass states could then make a $q\bar{q}$ nonet with members $K_0^*(1430)$ and $a_0(1450)$; in the isoscalar sector the three states $f_0(1370), f_0(1500)$ and $f_0(1710)$ could be, as originally proposed in \[10\], a superposition of the glueball and the two members of the isoscalar nonet.
   - **II. One nonet above 1 GeV**
     In this scheme the $\sigma$ and $\kappa$ with the parameters given are not considered as physical states to be classified along the lines we discuss here. The $q\bar{q}$ nonet is rather formed by $a_0(980)$ (or also $a_0(1450)$), $f_0(980), K_0^*(1430)$ and $f_0(1500)$ \[11,12\] whereas two higher mass nonets including $f_0(1370)$ have been proposed in \[11\]. The $\pi\pi$ S-wave is interpreted as being dominated by a very broad object, centered around 1 GeV, the lower part could be responsible for the $\sigma(500)$ effect. This broad state ($\Gamma>500$ MeV) has been proposed as representing the isoscalar glueball by various arguments \[13,12\].

There are states whose identity is in doubt as can be seen by the large uncertainty in mass and width estimated by the PDG: $\sigma(500), f_0(1370)$ with no single branching ratio or ratio of such numbers accepted by PDG and finally $\kappa$ or $K^*(800)$ not carried in the main listing of PDG. We will add a few remarks on these problematic states which will be of relevance for our discussion of $B$ decays.

**Isoscalar channel: $f_0(600)$ or $\sigma$ and $f_0(1370)$**

Most definitive experimental results on these states can be obtained from the $2 \rightarrow 2$ scattering processes $\pi\pi \rightarrow \pi\pi, KK, \eta\eta$ applying an energy independent partial wave analysis (EIPWA); in this case unitarity provides important constraints in the full energy
range. Recently, results on $D$ and $B$ decays as well as $p\bar{p} \to 3$ particles with higher statistics became available. There is no general constraint on the mass dependence of the amplitude which can be affected by various dynamical effects. So far, in these processes no EIPWA over the full energy range has been performed, so an optimal description of data for a particular model parametrization is selected. A promising new approach towards EIPWA in $D$-decays has been presented at this conference by Meadows [14].

Concerning the $\pi\pi$ interaction there is a general consensus that there exists indeed a broad state with the width of the order of the mass, but the parameters depend on the mass range considered, a feature which is known already since about 30 years.

1. **Low mass range $M_{\pi\pi} \lesssim 0.9 \ldots 1.2$ GeV.**

In this region the complex $\pi\pi$ amplitude moves along the unitarity circle to its top (phase $90^\circ$) where a rapid circular motion follows from $f_0(980)$. An early analysis has been performed by the Berkeley collaboration [15], they found a state, $\sigma$, with $M_\sigma = 660 \pm 100$ MeV, $\Gamma_\sigma = 640 \pm 140$ MeV. Recently, results from $D$-decays by E791 [16], FOCUS [17] and from $J/\psi \to \omega\pi\pi$ by BES [18] have been interpreted in terms of a $\sigma$ with similar mass, although good fits based on a $K$ matrix parametrization have been obtained without such a state [17]. On the theoretical side, parametrizations of such data using the low mass $\chi PT$ constraints lead to a low mass pole with $M_\sigma \sim 450$ MeV and $\Gamma_\sigma \sim 450 \ldots 600$ MeV (see, e.g. Refs. [19, 20] and the reports by Bugg and Pelaes [21]).

2. **Extended mass range $500 \leq M \leq 1800$ MeV**

In case of a broad state the parameters should be determined from the energy interval where its influence is important and this includes the inelastic region above 1 GeV.

All analyses of $\pi\pi$ scattering in this region find again one broad state, but with a higher mass than before, in a range around 1000 MeV and with large width $> 500$ MeV. The first analysis along these lines goes back again 30 years [22] and in Table 1 we list the pole positions from K matrix fits of various analyses. The fits by Estabrooks [23] refer to the four solutions of an EIPWA of elastic $\pi\pi$ scattering [24] as well as of the $\pi\pi \to K\bar{K}$ reaction. In all solutions of the EIPWA the $S$-wave amplitude above 1 GeV follows a circular path with some inelasticity in the Argand diagram ($Im T$ vs. $Re T$) which can be fitted by a broad resonance. Superimposed is a smaller circle corresponding to a resonance [23] with parameters close to what is known today as $f_0(1500)$. No additional pole, such as $f_0(1370)$, is seen in this analysis. A similar picture is found [12] for the inelastic channels $\pi\pi \to \eta\eta$ and $\pi\pi \to K\bar{K}$ comprising the broad background and $f_0(1500)$ with the interference pattern

$$
\begin{align*}
\pi\pi \to K\bar{K}: & \quad \text{background - } f_0(1500) \quad \text{constructive interference} \\
\pi\pi \to \eta\eta: & \quad \text{background - } f_0(1500) \quad \text{destructive interference}
\end{align*}
$$

This broad state is seen in a variety of processes and has been dubbed $f_0(1000)$ in [25]. Later arguments have been presented that this broad state may be a glueball [13, 12]. This state also appears in decay processes although it may happen that the higher mass tails are suppressed for dynamical reasons. As an example, we quote the study by BES [26] of the final state $J/\psi \to \omega K^+K^-$ where the large $S$-wave background ("$\sigma$") extends up to about 2 GeV. A significant flat background has also been observed recently in the gluon rich channel $J/\psi \to \gamma K\bar{K}$ by BES [27].
Apparently, the state $f_0(1370)$ shows up if reactions other than (1)-(3) in Table 1 without unitarity constraints are included in the fits. Whereas $f_0(980)$, "$f_0(1000)$" and $f_0(1500)$ are clearly seen as circles in the Argand diagrams, no such circle has ever been shown to exist for $f_0(1370)$. Before such a behaviour is demonstrated, this state could hardly be considered as established. The strong interference between background and $f_0(1500)$, leads to very different mass spectra, depending on the relative phase, which could easily simulate a "new state" $f_0(1370)$.

### TABLE 1. Position of broad state in the $T$ matrix of $\pi\pi$ scattering according to various $K$ matrix fits to data from reactions (1) $\pi\pi \rightarrow \pi\pi$, (2) $\pi\pi \rightarrow K\bar{K}$, (3) $\pi\pi \rightarrow \eta\eta, \eta\eta'$, (4) $p\bar{p}$ annihilation and (5) $J/\psi$ decays

| Authors                      | mass (MeV) | width (MeV) | channels |
|------------------------------|-----------|-------------|----------|
| CERN-Munich [22]             | 1049      | 500         | 1        |
| Estabrooks [23]              | 750       | 800-1000    | 1, 2     |
| Au, Morgan & Pennington [25] | 910       | 700         | 1, 2, 5  |
| Anisovich and Sarantsev [13] | 1530      | 1120        | 1, 2, 3, 4 |

We conclude that there is indeed a broad state in the isoscalar channel with decays into various 2-body final states but there is no standard form for its line shape. Different results on its mass emerge depending on whether the analytic parametrization is fitted to a small or a large mass range (corresponding to either a half resonance circle or an almost full circle) leading either to $\sigma(500)$ or "$f_0(1000)$". There can be little doubt that both results refer to the same state. Studies along path 1 should ultimately extend their parametrization to include higher mass inelastic channels, especially the EIPWA results by Estabrooks, whereas the analyses along path 2 should include the very low mass $\pi\pi$ data as well.

**Isospin $I = \frac{1}{2}$ channel: $\kappa(800)$ and $K_0^*(1430)$**

The elastic $K\pi$ scattering up to 1700 MeV has been studied some time ago by an experiment at SLAC [28] and the LASS experiment [29]. The $S$ wave phase shifts have been parametrized in terms of $K_0^*(1430)$ with a small inelasticity < 10% starting only above the inelastic threshold $M_{K\pi} \gtrsim M_{K\eta'} \sim 1450$ MeV and a slowly varying background with an effective range formula. This background phase in the considered range does not exceed about 50° and insofar it is a phenomenon quite different from the background in $\pi\pi$ scattering where the background phase reaches 90° below the first scalar resonance $f_0(980)$. We do not want to enter here into the discussion about a possible state $\kappa$ but point to different characteristics of the $K\pi$ amplitude in elastic scattering and decay relevant to our later discussion. For a theoretical analysis, see Büttiker et al. [30].

In weak decays like $D \rightarrow K\pi\mu\nu$ the $K\pi$ phase equals the one in elastic scattering according to the Watson theorem and this is nicely born out by the data (FOCUS [31]). If rescattering effects are small, then the Watson theorem is still applicable in purely hadronic decays and a recent example for this behaviour is $B \rightarrow J/\psi K\pi$ measured by BaBar [32]. On the other hand, in $D \rightarrow K\pi\pi$ the $K\pi$ phases determined by E791 [14] follow the trend as in elastic scattering below the inelastic $K\eta'$ threshold $M \sim 1400$ MeV, but with a relative shift of about 70°. The Argand diagram in Fig. 11 shows...
that the resonance circle related to $K_0^*(1430)$ is much smaller than the circle related to the background, which contrasts to elastic scattering with circles of comparable radii. Therefore the LASS parametrization does not represent the decay amplitude in an energy region beyond 1400 MeV.

![Diagram](image)

**FIGURE 1.** Energy independent partial wave analysis of the $I = \frac{1}{2}$ $K\pi$ $S$-wave using E791 data “$c_i$” and form factors $F_D$. Plotted are the rescaled quantities $S_i = c_i F_D \frac{q}{\sqrt{s}}$ (arbitrary units) to be compared with the elastic unitarity circle for $K\pi \rightarrow K\pi$ scattering.

**B-DECAYS: EXPERIMENTAL RESULTS ON SCALARS**

The $B$ branching ratios for the following scalar particles have been measured, for later comparison we present the results corrected for unseen channels, all in units of $10^{-6}$.

**Isospin $I=1$:** $a_0(980)$

So far only upper limits have been reported by BaBar $\cite{33}$,\footnote{After the conference results by Belle $\cite{34}$ became available which confirm the tight upper bounds for $a_0$ production: $B(B \rightarrow a_0^- K^+) < 1.6 \times 10^{-6}$ for the $\eta\pi$ channel.} see Tab.\footnote{2}

| $B$ decays into $a_0(980)$ corrected using $B(a_0 \rightarrow \eta\pi) = 0.85$; all numbers $\times 10^{-6}$. |  |
| --- | --- |
| $B^0 \rightarrow K^0 a_0^0$ | $< 9.2$ |
| $B^0 \rightarrow K^+ a_0^- a_0^0$ | $< 2.4$ |
| $B^+ \rightarrow K^0 a_0^0$ | $< 2.9$ |
| $B^0 \rightarrow K^+ a_0^- a_0^0$ | $< 4.6$ |

**Isospin $I = \frac{1}{2}$:** $K_0^*(1430)$

Total decay rates derived from BaBar $\cite{35}$ and Belle data $\cite{36}$ are given in Tab.\footnote{3} Belle, in a full Dalitz plot analysis using an isobar model ansatz finds two quite different solutions in $B^+ \rightarrow K_0^{*0} \pi^+$ corresponding to different interferences with a coherent background amplitude. Babar is inserting the LASS parametrization for the $K\pi$ phase in a larger energy interval up to $M \sim M_D$ and is then left with only one solution. As discussed above for $D \rightarrow K\pi\pi$ the behaviour of the $K\pi$ amplitude above 1400 MeV could be quite different from elastic scattering and a more general ansatz in this mass region seems appropriate. The situation is quite analogous to $f_0(980)$ in $\pi\pi$ interactions where the interference pattern of $f_0$ and background changes from one reaction to
another. It will be therefore important to clarify the existence of two solutions and to possibly exclude one of them by physical arguments.

**Isospin I=0: f_0(1500)**

Both Belle [36] and BaBar [37] see a peak in the K^+K^- Mass spectrum in B \rightarrow (K^+K^-)K. The mass and width are consistent with f_0(1500). However, no signal in the corresponding \pi\pi decay channel is observed despite the ratio of branching ratios \Gamma(f_0 \rightarrow K\bar{K})/\Gamma(f_0 \rightarrow \pi\pi) = 0.241 \pm 0.028 [7] is favourable for the \pi\pi channel. Therefore both collaborations suggested the existence of a new state, f_0(1500) or X(1500).

In a previous work [3] studying the Belle data [36] we argued that these phenomena are naturally explained by the existence of a broad background which interferes with f_0(1500): constructively in K^+K^- giving rise to the observed peak but destructively in \pi^+\pi^- leading to a vanishing signal. In our analysis we have represented the mass spectra as a superposition of three components f_0(980), f_0(1500) and a broad resonance as background, which fits the data well, see Figs. 2,3. This interference pattern is the same as in inelastic \pi\pi \rightarrow K\bar{K}, \eta\eta [12] and elastic \pi\pi scattering [23] (see above).

These signs are consistent with our hypothesis [12] that the background represents a broad glueball (flavour singlet) with mass in the 1 GeV region or above interfering with f_0(1500), which is close to a flavour octet state according to the considerations in [11,12].

Both collaborations find two solutions for the B \rightarrow Kf_0(1500) rate corresponding to different interference signs with the background. From the total charmless and the partial fractions we obtain the branching ratios in Tab. 4. According to our model Sol. II is the physical solution.

**Table 4.** B-decay rates (×10^{-6}) into f_0(1500)K (total rates using B(f_0(1500) \rightarrow K^+K^-) = 0.043).

|          | BaBar [35] | Belle [36] |
|----------|------------|------------|
| B(B \rightarrow f_0(1500)K) | 471.8 ± 51.3 | 223 ± 42 |
|              | Sol. I (bg - f_0) |          |
|              | 61.1 ± 14.4 | 29.9 ± 13.7 |
|              | Sol. II (bg + f_0) |          |

**Isospin I=0: f_0(980)**

f_0(980) was the first scalar particle observed in B-decays and the results obtained by the heavy flavor averaging group (HFAG) [38] are presented in Tab. 5. In these decay channels there is again some background contribution as in case of f_0(1500), so we expect two possible solutions corresponding to different interference signs. Note the negative interference in our fits in Figs. 2,3, also observed in J/ψ \rightarrow \phi\pi\pi by DM2 [39]. It would be important to study the possibility of a second solution besides the one in Tab. 5.
FIGURE 2. $\pi^+\pi^-$ mass spectrum in $B$-decays (BELLE [36]) in comparison with a model including $f_0(980)$, $f_0(1500)$ and a broad glueball ($gb$). Also shown are the individual resonance terms. The background ($gb$) in this fit interferes destructively with both $f_0(980)$ and $f_0(1500)$.

FIGURE 3. $K^+K^-$ mass spectrum in $B$-decays (BELLE [36]) in comparison with the model amplitude, see Fig. (2). Here $f_0(1500)$ interferes constructively with the background.

Other results on scalars

$f_0(1370)$: A $2\sigma$ signal has been observed by Belle [36], not so by BaBar [35].

$\sigma(600)$: No obvious peak near threshold is visible as in $D \rightarrow 3\pi$. For our discussion of scalars it would be interesting to obtain the rate for $B \rightarrow \sigma K$ (or a limit).

$\kappa(800)$: A $K\pi$ background in $K\pi\pi$ has been observed by Belle [36] but a fit with a $\kappa$ particle was not successful.
$a_0(1450)$: This state has not been seen yet.

### TABLE 5. $B$-decay rates ($\times 10^{-6}$) into $f_0(980)K$, for $f_0(980) \to \pi\pi$ and total rate using $\Gamma(f_0(980) \to \pi\pi)/\Gamma_{\text{tot}} \sim 0.8$.

| $f_0(980) \to \pi\pi$ | $f_0(980) \to \text{all}$ |
|-----------------------|--------------------------|
| $B(B^+ \to f_0(980)K^+)$ | $13.2 \pm 1.6$ | $16.5$ |
| $B(B^0 \to f_0(980)K^0)$ | $8.25 \pm 1.5$ | $10.3$ |

**B-decays into scalars: theoretical expectations**

The theoretical considerations to some extent follow the ideas developed earlier for $B$-decays into pseudoscalar (P) and vector (V) particles. We outline here two complementary approaches.

**Phenomenological amplitudes**

The decay rates are expressed in terms of a set of phenomenological amplitudes including the gluonic penguin, the electroweak tree amplitudes and others. Such a scheme has been successfully applied to the decays $B \to PP, PV$ [40, 41].

Here we apply a scheme of this kind [3], but in this exploratory phase for scalars with moderate statistics we restrict ourselves to including only the dominant penguin diagrams and neglect in particular the tree diagrams which give rise to corrections at the 20% level. We then consider in this scheme the three $q\bar{q}$ processes with the same amplitude as well as the gluonic amplitude

$$b \to s\bar{u}, \quad b \to s\bar{d}, \quad b \to s\bar{s}, \quad b \to s\bar{g}. \tag{3}$$

These processes together with the recombination of the spectator quark give rise to 2-body decays $B \to xy$ where $x, y$ are mesons out of the flavour $U(3)$ nonets $A$ and $B$. Given the members of these multiplets with a particular mixing angle the decay amplitudes can be given in terms of the following parameters: the penguin amplitude $p_{AB}$ with $s \to x$, the exchange amplitude $\beta_{AB}p_{AB}$ for $s \to y$ and $\gamma_{AB}p_{AB}$ for the gluonic amplitude. For a more detailed discussion, see Ref. [3], here we just adress for illustration the decay $B^+ \to \eta'K^{*+}$ for the mixing $\eta' = (u\bar{u}, d\bar{d}, 2s\bar{s})/\sqrt{6}$. The decay amplitude is derived from the penguin amplitudes as in Fig. 4 and reads

$$T = \frac{1}{\sqrt{6}} (1 + 2\beta_{PV} + 4\gamma_{PV}) p_{PV} \tag{4}$$

A consequence of this penguin dominance model are various symmetry relations, especially the $I = \frac{1}{2}$ rule: The final state of processes [3] has $I = 0$ and therefore the final state of $B$ decay has the isospin of the spectator, for $B^+, B^0$ this is $I = \frac{1}{2}$, which is also realized in our amplitudes [3], see also Tab. 6 below.
Application to B-decays into pseudoscalars

As a test of this penguin dominance model we have compared first with data on the decays $B \to PP$, $B \to PV$ [3]. In Tab. 6 this comparison is repeated with new data compiled by HFAG [38]. In col. 2 we show our predictions for 12 decay rates of $B^+$ in terms of the parameters $p_{PP}, p_{VP}, \gamma_{PP}, \gamma_{VP}, \beta_{VP}$ and the corresponding 12 rates for $B^0$ obtained after multiplication by the lifetime ratio $\tau(B^0)/\tau(B^+) = 0.921$. From col. 2 various symmetry relations can be obtained, especially the $I = \frac{1}{2}$ rule (favouring charged $\pi$ or $\rho$ over the neutral decays by a factor 2) for the doublets

$$(K^0 \pi^0), (K^+ \pi^0); (K^+ \pi^-), (K^0 \pi^0); (K^{*0} \pi^+), (K^{*+} \pi^0); (K^{*+} \pi^-), (K^{*0} \pi^0)$$

$$(\rho^+ K^0), (\rho^0 K^+); (\rho^- K^+), (\rho^0 K^0)$$

These relations work well, except for one case where the rate for $K^{*0} \pi^0$ is significantly (4.3σ) below the expectation; however, the statistics is very low in this case. Furthermore, there are SU(3) relations between $K^{*0} \pi^0$ and $\phi K$, and also between $\rho K$ and $\omega K$ which work reasonably well.

For a full description we made some simplifying assumptions $\beta_{VP} = -1, \gamma_{VP} = \gamma_{PP}$ which can be removed if necessary with improving statistics. The remaining 3 parameters $p_{PP}, p_{VP}, \gamma_{PP}$ have been determined from 3 input rates. Remarkably, with the data of increased precision obtained in the last year [38] the agreement with the predictions has generally improved in comparison to our earlier results in [3] (2 exceptions with deviations of $> 3\sigma$).

B-decays into scalar particles

After the success of this simple penguin dominance model we take it over to the decays with scalar particles $B \to PS$ and $B \to VS$. We denote the members of the scalar multiplet by $a, K_{sc}^+, f_0, f'_0$, and define the mixing angle by $f_0 = n\bar{n}\sin \varphi_s + s\bar{s}\cos \varphi_s$, $f'_0 = n\bar{n}\cos \varphi_s - s\bar{s}\sin \varphi_s$, where $n\bar{n} = (u\bar{u} + d\bar{d})/\sqrt{2}$. Then our predictions [3] for scalars are given in Tab. 7. Given the decay branching ratios into scalars one can check any scenario for the multiplet of scalar particles. Hopefully, the symmetries implied by
TABLE 6. Branching ratios for $B$ decays into pseudoscalar (P) and vector (V) particles (cols. 3,4,6,7) and amplitudes (col. 2) as in Eq. (4) with $\gamma_P, \gamma_P^\prime$ and $\beta_P$ for gluonic and interchange processes, $p_{PP}$, $p_{VP}$ set to 1; cols. 3: $\gamma_P = \gamma_P^\prime = 0.3$, $\beta_P = -1$, $|p_{PP}|^2 = 24.1 \times 10^{-6}$, $|p_{VP}|^2 = 11.4 \times 10^{-6}$. Experimental Data from HFAG, July 2005.

| $B^+ \rightarrow PP$ | $p_{PP} = 1$ | $B_{th}[10^{-6}]$ | $B_{exp}[10^{-6}]$ | $B^0 \rightarrow PP$ | $B_{th}[10^{-6}]$ | $B_{exp}[10^{-6}]$ |
|----------------------|--------------|----------------|----------------|----------------------|--------------|----------------|
| $K^0 \pi^+$          | 1            | 24.1 $\pm$ 1.3 | 22.2           | 16.2 $\pm$ 0.8      |
| $K^+ \pi^0$          | $\frac{1}{\sqrt{2}}$ | 12.1          | 11.1           | 11.5 $\pm$ 1.0      |
| $K^+ \eta$           | $\frac{1}{\sqrt{3}} \gamma_{PP}$ | 0.7           | 2.6 $\pm$ 0.5  | 0.7                  | < 2.0        |
| $K^+ \eta'$          | $\frac{1}{\sqrt{6}} (3 + 4 \gamma_{PP})$ | 70.8 $\pm$ 3.4 | 65.3           | 68.6 $\pm$ 4.2      |

| $B^+ \rightarrow VP$ | $p_{VP} = 1$ | $B^0 \rightarrow VP$ |
|----------------------|--------------|-------------------|
| $K^{0*} \pi^+$       | 1            | $K^{0*} \pi^+$    |
| $K^{+*} \pi^0$       | $\frac{1}{\sqrt{2}}$ | $K^{+*} \pi^0$   |
| $K^{+*} \eta$        | $\frac{1}{\sqrt{3}} \gamma_{VP}$ | $K^{+*} \eta$  |
| $K^{+*} \eta'$       | $\frac{1}{\sqrt{6}} (3 + 4 \gamma_{VP})$ | $K^{+*} \eta'$  |

| $B^0 \rightarrow VP$ |
|----------------------|
| $p_{VP} = 1$ |

**TABLE 7.** Dominant contributions for $B$ decays into scalar (S) + pseudoscalar (P) or vector (V) particles: penguin amplitudes $p_{PS}$ (normalized to 1 in each sector), exchange and gluonic amplitudes $\beta_V$ for scalar mixing angle $\phi_S$; in brackets results for $\sin \phi_S = 1/\sqrt{3}$ ($\phi_S = \phi_P$); cols. 3: upper sign for $B^0$, lower sign $B^+$. 

| $B^0 \rightarrow$ | $B^+ \rightarrow$ | normalization to $p_{PS} = 1$ | $B^0 \rightarrow$ | $B^+ \rightarrow$ | normalization to $p_{PS} = 1$ |
|-------------------|-------------------|----------------|----------------|----------------|----------------|
| $P + S$            | $P + S$            | $p_{PS} = 1$  | $V + S$            | $V + S$            | $p_{PS} = 1$  |
| $K^{0*} a^-$       | $K^{0*} a^+$      | 1             | $K^{+*} a^-$       | $K^{+*} a^+$      | 1             |
| $K^0 a^0$          | $K^+ a^0$         | $\frac{1}{\sqrt{2}}$ | $K^0 a^0$          | $K^+ a^0$         | $\frac{1}{\sqrt{2}}$ |
| $K^0 f_0$          | $K^+ f_0$         | $\frac{1}{\sqrt{2}} (1 + 2 \gamma_{PS}) \sin \phi_S$ | $\frac{1}{\sqrt{2}} (1 + 2 \gamma_{PS}) \sin \phi_S$ | $\frac{1}{\sqrt{2}} (1 + 2 \gamma_{PS}) \sin \phi_S$ | $\frac{1}{\sqrt{2}} (1 + 2 \gamma_{PS}) \sin \phi_S$ |
| $K^0 f_0$'         | $K^+ f_0'$        | $\frac{1}{\sqrt{2}} (1 + 2 \gamma_{PS}) \cos \phi_S$ | $\frac{1}{\sqrt{2}} (1 + 2 \gamma_{PS}) \cos \phi_S$ | $\frac{1}{\sqrt{2}} (1 + 2 \gamma_{PS}) \cos \phi_S$ | $\frac{1}{\sqrt{2}} (1 + 2 \gamma_{PS}) \cos \phi_S$ |
| $\pi^- K^{0*}$     | $\pi^+ K_0^{0*}$  | $\beta_{PS}$   | $\rho^- K^{0*}$    | $\rho^+ K_0^{0*}$  | $\beta_{PS}$   |
| $\pi^0 K^{0*}$     | $\pi^0 K_0^{0*}$  | $\frac{1}{\sqrt{2}} \beta_{PS}$ | $\rho^0 K^{0*}$    | $\rho^0 K_0^{0*}$  | $\beta_{PS}$   |
| $\eta K^{0*}$      | $\eta K_0^{0*}$   | $\frac{1}{\sqrt{2}} (1 + \beta_{PS} + \gamma_{PS})$ | $\omega K^{0*}$    | $\omega K_0^{0*}$  | $\beta_{PS}$   |
| $\eta' K^{0*}$     | $\eta' K_0^{0*}$  | $\frac{1}{\sqrt{2}} (2 + \beta_{PS} + 4 \gamma_{PS})$ | $\phi K^{0*}$      | $\phi K_0^{0*}$   | $\beta_{PS}$   |

Penguin dominance (isospin, SU(3)) inherent in Tab. 7 will help in selecting the correct assignments of scalar particles. The parameters we have at our disposal are for $B \rightarrow PS$: $p_{PS}, \gamma_{PS}, \gamma_{PS}, \beta_{PS}$ and for $B \rightarrow VS$: $p_{VS}, \gamma_{PS}, \beta_{VS}$. In our first analysis [2] we used initially, in analogy to the pseudoscalars, $\beta_{PS} = 1$, $\beta_{VS} = -\beta_{PS}$, $\gamma_{PS} = \gamma_{VS} = \gamma_{SP}$. 


Comparison with experimental results on scalars in B decays

Considering first the multiplet $\sigma, \kappa, f_0(980), a_0(980)$ along scenario I we note that only $f_0(980)$ has been observed so far. For a meaningful test one would need a measurement of the rates for $B \to K\sigma$ and $B \to \pi\kappa$ which should be possible for a given parametrization.

On the other hand, the decay rates for all members of the multiplet along scenario II $f_0(980), a_0(980), K_0^\ast(1430), f_0(1500)$ have actually been measured (upper limit for $a_0$ only). According to our scheme with penguin dominance we should describe these four rates by 3 parameters: $\sigma_{PS}, \gamma_{PS}$ and $\beta_{PS}$.

In a first attempt in 2004 we analysed the data assuming as in case of pseudoscalars $|\beta_{PS}| = 1$. Then we expected for the decay $B(B \to Ka_0^\pm) \gtrsim 11.0 \times 10^{-6}$ (±50%) The new upper limits from BaBar in Tab. 2 are below this expectation. From Tab. 7 we find $B(B \to K_0^\ast \pi^\pm)/B(B \to Ka^\pm) = |\beta_{PS}|^2$. The new data require $|\beta_{PS}| \sim 2.7 \ldots 4.6$, or, from averages using the $I = 1/2$ rule $|\beta_{PS}| \gtrsim 2$. The production of a scalar with the spectator is suppressed against production from $s$-quark.

Until now, there are still considerable experimental uncertainties, especially the ambiguities in the $K_0^\ast(1430)$ rates and the missing $a_0$ rate. If we choose $|\beta_{PS}| = 2$ then we find with $B(B \to K_0^\ast \pi^\pm) \sim 12 \times 10^{-6}$ (if we include the lower $K_0^\ast$ mass), for $B(B \to a_0^+ K^0) \sim 3 \times 10^{-6}$ and $B(B \to Kf_0(980)) \sim 13 \times 10^{-6}$ four solutions in $(\beta, \gamma)$. For $\beta = -2, \gamma = 2$ we find $B(B \to Kf_0(1500)) \sim 25 \times 10^{-6}$ which compares well with Sol. II in Tab. 4. So there is no difficulty in the moment with the multiplet along path II considered. The tests will hopefully become more restrictive with improved data and with measurements of other channels like $K_0^\ast(1430)\eta, K_0^\ast(1430)\eta'$ and $B \to V^+\eta$ scalars.

QCD-improved factorization approximation

In this complementary theoretical investigation one aims at an absolute prediction of rates for scalar particles $[42, 43, 44]$. This follows the approach applied before to decays $B \to PP, VP$ $[45]$. In the recent work $[44]$ one includes perturbative QCD corrections to the common factorization ansatz but needs to include various non-perturbative objects: formfactors, light cone distribution amplitudes and decay constants where results for scalars are derived from QCD sum rules. In scenario I $\sigma, \kappa, a_0(980), f_0(980)$ are taken as $q\bar{q}$ ground states and $a_0(1450), K^*(1430), f_0(1500)$ as $q\bar{q}$ excited states. In scenario II it is assumed that the low mass multiplet is build of $q\bar{q}\bar{q}\bar{q}$ states for which no quantitative predictions can be given, whereas the $q\bar{q}$ ground state multiplet includes $a_0(1450), K_0^\ast(1430)$ and a second multiplet is around 2 GeV.

An early calculation $[42]$ predicted a very small rate for $B^0 \to a_0^0 K^-$ which turned out successful. The recent predictions $[44]$ concern decays into $a_0(980), f_0(980)$, also $K^*(1430)$ and $a_0(1430)$. Within scenario I the results on the low mass multiplet are satisfactory whereas the higher mass particles require the low mass solutions with $B(B^- \to K^*(1430)^-\pi^+) < 10 \times 10^{-6}$. In scenario II the $K_0^\ast$ rates are about twice as large as before, but still smaller than some experimental results.

If this large $K_0^\ast$ rate is correct, then scenario I is excluded and there are no predictions
for the light mesons with $M \lesssim 1$ GeV. It will be important to know the predictions for the other states $\sigma, \kappa$ to compare with, likewise predictions for $f_0(1500)$ and the other isoscalar meson.

**CONCLUSIONS**

1. **Experimental results on decays $B \to Scalar +X$**
   By now $f_0(980), a_0(980), K_0^*(1430)$ and $f_0(1500)$ have been measured in $B$-decays. Discrete ambiguities are found for $K_0^*(1430), f_0(1500)$ (how about $f_0(980)$?) and emerge naturally in coherent superpositions. A clarification is important, possibly these ambiguities can be resolved by physical arguments (comparison with elastic scattering phases, isospin relations fulfilled within $\sim 20\%$).

2. **Model with gluonic penguins dominating and $B \to S + X$ amplitudes**
   This model continues to work well for $B \to PP, VP$ within $\sim 20\%$ or better, especially the $I = \frac{1}{2}$ rule and other SU(3) relations are generally successful. The method has the potential to test the multiplet structure in the scalar sector. Present data within their ambiguities are consistent with a $q\bar{q}$ multiplet $f_0(980), a_0(980), K_0^*(1430), f_0(1500)$. Further tests are possible with $B \to K_0^*(1430)\eta$ (or $\eta'$) as well as $VS$ rates. The possibility of a light multiplet with $\sigma, \kappa$ can be tested once data on $B \to \sigma K, \kappa \pi$ become available.

3. **Factorization approach for $B$-decays into scalar particles**
   Using QCD sum rules to obtain nonperturbative quantities some absolute predictions have been obtained, a successful one concerns the decay into $a_0(980)$. Further distinctions between different scenarios depend on the magnitude of the ambiguous $K_0^*(1430)\pi$ rate. It will be important to have predictions for the other members of the considered multiplets, especially for $B \to \sigma K, \kappa \pi$, as well as for heavier isoscalars.

4. **Broad state: a respectable glueball candidate and the $X(1500), f_X(1500)$ puzzle.**
   In the $\pi\pi$ channel there is a broad state with $\Gamma \sim M$. It is plausible that $\sigma(600)$ and $f_0(1000)$ refer to the same object. The puzzles with $X(1500), f_X(1500)$ are resolved by taking into account the interference of $f_0(1500)$ with a broad background. The relative signs are explained by taking the background as flavour singlet, in agreement with the glueball hypothesis, and $f_0(1500)$ as a flavour octet state. The same interference phenomenon is known from processes $\pi\pi \to \pi\pi, \eta\eta, K\bar{K}$.

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**NOTE ADDED**

After this conference a paper by Gronau and Rosner [46] appeared with isospin relations between pairs of $B^0$ and $B^+$ 2-body decays as well as 3-body decays also basing on the
dominance of penguin amplitudes.

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