SOFIA/FORCAST Observations of the Luminous Blue Variable Candidates
MN 90 and HD 168625

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Abstract

We present Stratospheric Observatory for Infrared Astronomy (SOFIA)/Faint Object infraRed CAmera for the SOFIA Telescope (FORCAST) imaging of the circumstellar dust shells surrounding the luminous blue variable candidates MN 90 and HD 168625 to quantify the mineral abundances of the dust and to constrain the evolutionary state of these objects. Our image at 37.1 μm of MN 90 shows a limb-brightened, spherical dust shell. A least-squares fit to the spectral energy distribution of MN 90 yields a dust temperature of 59 ± 10 K, with the peak of the emission at 42.7 μm. Using 2-Dust radiative transfer code, we estimate for MN 90 that mass loss occurred at a rate of (7.3 ± 0.4) × 10^{-7} M_☉ yr^{-1} × (v_{exp}/50 km s^{-1}) to create a dust shell with a dust mass of (3.2 ± 0.1) × 10^{-2} M_☉. Our images between 7.7 and 37.1 μm of HD 168625 complement previously obtained mid-IR imaging of its bipolar nebulae. The SOFIA/FORCAST imaging of HD 168625 shows evidence for the limb-brightened peaks of an equatorial torus. We estimate a dust temperature of 170 ± 40 K for the equatorial dust surrounding HD 168625, with the peak of the emission at 18.3 μm. Our 2-Dust model for HD 168625 estimates that mass loss occurred at a rate of (3.2 ± 0.2) × 10^{-7} M_☉ yr^{-1} to create a dust torus/shell with a dust mass of (2.5 ± 0.1) × 10^{-2} M_☉.

Key words: circumstellar matter – stars: individual (HD 168625, MN 90) – stars: massive – stars: mass-loss

1. Introduction

It is widely recognized that luminous blue variables (LBVs) represent a post-main-sequence phase in which massive stars (initial mass \(M_\star \geq 20 M_☉\); Langer et al. 1994) lose a considerable amount of mass via giant eruptions and minor outbursts. From the expansion velocities of known LBV nebulae, a dynamical age of a few 10^4 years is usually inferred, which points to a very short-lived evolutionary phase—only about 40 are known (Clark et al. 2005; Weis 2011; Nazé et al. 2012). Although the category is still not unambiguously defined, these objects generally exhibit a high luminosity (\(\geq 10^{5.5} L_☉\)), low amplitude photometric variability (~0.1 mag) on timescales ranging from weeks to months, and a larger, irregular photometric variability, called S Dor variability, with amplitudes of 1–2 mag occuring on timescales of years to decades with mass-loss rates of \(\sim 10^{-5}–10^{-4} M_☉ yr^{-1}\). In addition, some LBVs exhibit giant eruptions, η Car being the most famous example (Humphreys et al. 1999). These giant eruptions are responsible for producing circumstellar nebulae with sizes of up to 1–2 pc and expansion velocities anywhere from 10 km s^{-1} to several hundred km s^{-1} for most LBVs (Weis 2011) that are then shaped by wind–wind interactions (van Marle et al. 2007). In rare cases, very fast speeds have been seen, reaching as high as 6000 km s^{-1} in the case of η Car (Smith 2008). These nebulae can have various morphologies; Weis (2011) estimates 50% are bipolar, 40% are spherical, and 10% are irregular. The bipolar nebulae may be formed by density gradients in the wind (Frank et al. 1995), different mass-loss episodes in which the wind changes from equatorial to polar during the bistability jump (Smith et al. 2004), or the rotation of the star (Dwarkadas & Owocwi 2002; Smith & Townsend 2007). Thus, the morphology of the nebula discloses the mass-loss history and evolutionary stage of the central star and the circumstellar environment.

In this work, we present 5–40 μm mid-IR observations of the two compact nebulae, MN 90 and HD 168625 with the Faint Object infraRed CAmera for the Stratospheric Observatory for Infrared Astronomy (SOFIA) Telescope (FORCAST; Herter et al. 2012) instrument on board the NASA SOFIA (Becklin et al. 2007; Gehrz et al. 2009; Young et al. 2012). By imaging these nebulae at a range of wavelengths, we can study their structure, estimate the dust composition, and quantify the dust temperature and total mass. These parameters will help to determine the physical properties of the circumstellar environments and to constrain the importance of eruptive mass loss in post-main-sequence stellar evolution. In Section 2, we summarize the observations and data reduction strategies. Section 3 describes the axisymmetric radiative transfer code 2-Dust and the derived dust geometry parameters and inferred mass-loss histories. We discuss the results of our analysis in Section 4 and present the conclusions in Section 5.

MN 90 (central star 2MASS J18455593-0308297) was discovered and cataloged by Gvaramadze et al. (2010) using the Multiband Imaging Photometer (MIPS; Rieke et al. 2004) on board the Spitzer Space Telescope (Werner et al. 2004; Gehrz et al. 2007) in the MIPS Galactic Plane Survey (MIPSGAL; Carey et al. 2009), which mapped 278 deg^2 of the inner Galactic plane: -65° < l < -10° and 10° < l < 65° for \(|b| < 1°\). It is one of a large number of similar shells found in MIPSGAL images that resemble the circumstellar nebulae of LBVs and late WN-type Wolf–Rayet stars (WNL). The lack of optical counterparts for most of them indicates that they are highly obscured (Wachter et al. 2010). Follow-up spectroscopy of some of the other MIPS Nebulae has revealed them to be LBVs, candidate LBVs, or early-type supergiants (see the summary list in Kniazev et al. 2015). MN 90 appears nearly circular as projected on the
sky and appears to be a limb-brightened shell with a star at the center. The star is undetected in Swift UV images, Palomar Observatory Sky Survey visual images, and the ground-based visual images used to make the HST Guide Star Catalog. The distance to MN 90 is unknown and there is little information about its physical parameters. Wachter et al. (2010) included MN 90 along with a large sample of numerous similar shells for follow-up spectroscopy but ultimately did not report any spectra for this particular star. Based on the analysis of other stars in their sample, they grouped MN 90 along with other shells for which they predict the stars are early type. Nazé et al. (2012) did not detect any X-ray emission from MN 90 in their XMM-Newton survey of a sample of known and candidate LBVs. Mizuno et al. (2010) list MN 90 as MGE029.5086-00.2090, but other than reporting a MIPS-GAL flux at 24 μm, there is nothing more specific about the central star. We are unaware of any other imaging or spectroscopy of MN 90 that may have been obtained. Hereafter, we will use “MN 90” to refer to both the nebula and the central star.

HD 168625 (IRAS 18184–1623) was first identified as a candidate LBV by Chentsov & Luad (1989), who classified it as spectral type B5.6 ± 0.3 with $T_{\text{eff}} \approx 13,000$ K. Its spectral type seems to vary from B2 (Popper & Seyfert 1940) to B8 (Morgan et al. 1955), although no dramatic light-variations have been reported in the last 40 years (van Genderen et al. 1992; Sterken et al. 1999). The lack of evidence for large variations kept HD 168625 from being classified as an LBV. However, it was found to be LBV-like by Hutsemekers et al. (1994) who, using near-infrared (near-IR) and visible imaging and spectroscopy, found a high mass-loss rate and a shell with two regions: an inner $10'' \times 13''$ elliptical ring and a perpendicular outer horn-shaped region suggesting a bipolar outflow. Nota et al. (1996) used deeper Hα imaging of the nebula to identify faint filaments in the bipolar structure that extended to $16'' \times 21''$, indicating that an LBV-like major outburst occurred $\sim 10^3$ years ago. Given its curious characteristics, HD 168625 has been the focus of several additional studies. Meixner et al. (1999) included it in their large, mid-infrared (mid-IR) protoplanetary nebula (PPN) candidates survey and imaged it at 8.8, 12.5, and 20.6 μm revealing a toroidal dust shell. From mid-IR images at 4.7, 10.1, 11.6, and 19.9 μm, Robberto & Herbst (1998) used an analytical spherical model to derive a dust temperature of 135 K and a dust mass of $2.8 \times 10^{-3}$ $M_\odot$. Similarly, Pasquale et al. (2002) used mid-IR imaging at 4 and 11 μm to derive a dust temperature of 113 K, and a nebular expansion velocity of 19 km s$^{-1}$ from ground-based echelle spectra. O’Hara et al. (2003) modeled the morphology of the toroidal dust region using 2-Dust and found a dust mass of $2.5 \pm 0.1 \times 10^{-2}$ $M_\odot$. Mahy et al. (2016) used far-infrared (far-IR) imaging and spectroscopy with optical spectra to constrain the CNO abundances of HD 168625 and the surrounding nebula to determine that the central star had an initial mass between 28 and 33 $M_\odot$ and lost its material after the blue supergiant (BSG) phase. Smith (2007) presented Spitzer images showing that the bipolar lobes and torus of HD 168625 were actually a triple-ring system that closely resembled the ringed nebula around SN 1987A. He pointed out that a single rotating star could potentially eject an equatorial torus even if it is not rotating at the critical speed. Presumably this can occur because the stars approach or violate the classical Eddington limit during their giant eruptions when the mass is ejected (see, e.g., Smith & Townsend 2007) allowing the star’s rotation to be more influential at the resulting lower effective gravity. Taylor et al. (2014) found no evidence for a binary companion to HD 168625 from radial velocity monitoring and a modest rotation speed of 53 km s$^{-1}$. The presence of a possible companion star was detected by Aldoretta et al. (2015) using interferometric observations. A wide-orbit companion with a projected separation of 1′′15 was later confirmed by Martayan et al. (2016) using adaptive optics images, but there is no evidence that it is gravitationally bound to HD 168625 and it is too distant to have any impact on the shaping of the nebula. The role companions might play in the formation and evolution of LBV and LBV-like objects is still not well understood.

2. Observations and Data Reduction

The targets were observed with SOFIA/FORCAST during Guest Investigator (GI) Cycles 2 and 3. Descriptions of the SOFIA Observatory and its science instrument (SI) suite have been given by Becklin et al. (2007), Gehrz et al. (2009), and Young et al. (2012).

FORCAST is a dual-channel mid-IR imager covering the 5–40 μm range. Each channel uses a 256 × 256 pixel array and provides a distortion-corrected 3′′2 × 3′′2 field of view with a scale of 0′′768 pix$^{-1}$. The Short Wave Camera uses a Si:As blocked-impurity band (BBB) array optimized for $\lambda < 25$ μm, while the Long Wave Camera’s Si:Sb BBB array is optimized for $\lambda > 25$ μm. Observations were taken in standard two-position chop-and-nod mode with the direction of the nod matching the direction of the chop (NMC). The data were reduced by the SOFIA Science Center using the FORCAST Redux v1.0.1/β and v1.0.6 pipelines ( Clarke et al. 2015) for HD 168625 and MN 90, respectively. After correction for bad pixels and droop effects, the pipeline removed sky and telescope background emission by first subtracting chopped image pairs and then subtracting nodded image pairs. The resulting positive images were aligned and merged. The merged images were then coadded using a robust mean.

We observed MN 90 on UT 2015 July 3 during Guest Investigator (GI) Cycle 3 using the F371 filter ($\lambda_0 = 37.1$ μm, $\Delta \lambda = 3.3$ μm). The total coadded exposure time for the observation of MN 90 was 1553 s (25.9 minutes). Table 2 summarizes the observed flux from MN 90. Observations of the asteroid Vesta provided the flux calibration and PSF, with a near-diffraction-limited FWHM at 37.1 μm of 3′′6.

We observed HD 168625 on UT 2014 June 13 during Guest Investigator (GI) Cycle 2 using eight different filters, which are summarized in Tables 1 and 2. Observations of Beta Andromedae provided the flux calibration and PSF.

2.1. Spectral Energy Distributions (SEDs)

We present the IR SEDs of MN 90 and HD 168625 in Figures 1 and 2, respectively. To supplement our newly acquired SOFIA/FORCAST photometry, we also gathered archival data from the NASA/IPAC Infrared Science Archive (IRSA; Berriman 2008) database. These include photometry from the Two Micron All-Sky Survey (2MASS; Skrutskie et al. 2006) at 1.25, 1.65, and 2.17 μm, the AKARI satellite (Murakami et al. 2007) at 9 and 18 μm, the Wide-field Infrared Survey Explorer (WISE; Wright et al. 2010) at 3.4, 4.6, 12, and 22 μm, the Midcourse Space Experiment (MSX; Egan et al. 2003) at 8.3, 12.1, 14.7, and 21.3 μm the Spitzer MIPS at...
Figure 1. Observed and model SEDs of MN 90. The reddened model SED is shown as a solid blue line. The dashed lines are the best fitting \( Q \lambda \beta \), functions with an assumed power-law emissivity \( Q \lambda \propto \lambda^{-\beta} \), which yields \( T_d = 59 \pm 10 \text{ K} \), \( \beta = 0.76 \pm 1.07 \) with the peak of the emission at \( \lambda = 42.7 \mu \text{m} \). Photometry data points are from this work (SOFIA) and archival databases.

### Table 1

Summary of SOFIA/FORCAST Observations of HD 168625

| Filter | \( \lambda_0 \) (\( \mu \text{m} \)) | \( \Delta \lambda \) (\( \mu \text{m} \)) | Exp. Time (s) | PSF FWHM (arcsec) |
|--------|----------------|----------------|--------------|------------------|
| F077   | 7.7            | 0.47           | 30           | 2'5              |
| F111   | 11.1           | 0.95           | 30           | 2'5              |
| F197   | 19.7           | 5.5            | 16           | 2'7              |
| F253   | 25.3           | 1.86           | 25           | 3'0              |
| F315   | 31.5           | 5.7            | 25           | 3'1              |
| F336   | 33.6           | 1.9            | 31           | 3'1              |
| F348   | 34.8           | 3.8            | 30           | 3'4              |
| F371   | 37.1           | 3.3            | 26           | 3'5              |

Table 2

SOFIA/FORCAST Fluxes from MN 90 and HD 168625

| Filter | Flux \( 10^{-12} \text{(W m}^{-2} \text{)} \) | Error \( 10^{-12} \text{(W m}^{-2} \text{)} \) |
|--------|-------------------|------------------|
| MN 90  |                   |                  |
| F371   | 2.74              | 0.01             |
| HD 168625 |                 |                  |
| F077   | 14.75             | 0.04             |
| F111   | 15.32             | 0.05             |
| F197   | 46.76             | 0.18             |
| F253   | 28.00             | 0.06             |
| F315   | 22.51             | 0.05             |
| F336   | 26.03             | 0.05             |
| F348   | 19.43             | 0.03             |
| F371   | 13.65             | 0.04             |

24 \( \mu \text{m} \), and the Spitzer Infrared Array Camera (IRAC) Galactic Legacy Infrared Midplane Survey Extraordinaire I (GLIMPSE I; Benjamin et al. 2003; Churchwell et al. 2009) program at 3.6, 4.5, 5.8, and 8 \( \mu \text{m} \). Photometry from our SOFIA/FORCAST images and the Herschel (Pilbratt 2003) Photoconductor Array Camera and Spectrometer (PACS; Poglitsch et al. 2010) at 70, 100, and 160 \( \mu \text{m} \) were obtained by using aperture photometry after sky background subtraction. For MN 90, we used an aperture of 30'' and a sky annulus with an inner radius of 31.5'' and outer radius of 35''. For HD 168625, we used an aperture of 20'' and a sky annulus with an inner radius of 21.5'' and outer radius of 25''. Note that in the longer wavelength Herschel PACS/SPIRE images of MN 90 from 160 to 500 \( \mu \text{m} \) the dust shell is no longer distinguishable above bright diffuse background emission. Only IRAC 5.8 \( \mu \text{m} \) photometry of the central star was available for HD 168625, the central star saturated the IRAC detector in the 3.6 and 4.5 \( \mu \text{m} \) images, while warm circumstellar dust saturated the detector at 8.0 \( \mu \text{m} \). For HD 168625, we further include the Infrared Astronomical Satellite (IRAS; Neugebauer et al. 1984) Low Resolution Spectrometer (LRS) spectra from Volk & Cohen (1989).

We model the dust shell flux as equilibrium thermal emission from dust grains all at a single radius \( r_d \) from the star. We assume the grains’ emissivity behaves as a power law with \( Q_\lambda \propto \lambda^{-\beta} \). For MN 90, a least-squares fit of a \( B_\lambda(T_d) \) curve modified with this emissivity yields \( T_d = 59 \pm 10 \text{ K} \), \( \beta = 0.76 \pm 1.07 \), with the peak of the emission at \( \lambda = 42.7 \mu \text{m} \).

For HD 168625, a least-squares fit of a \( B_\lambda(T_d) \) curve modified with this emissivity \( Q_\lambda \propto \lambda^{-\beta} \) yields \( T_d = 170 \pm 40 \text{ K} \), \( \beta = -0.33 \pm 1.04 \), with the peak of the emission at \( \lambda = 18.3 \mu \text{m} \).

2.2. Imaging of MN 90

Our FORCAST 37.1 \( \mu \text{m} \) image of MN 90 is shown in Figure 3. The nebula is clearly resolved, with a radius of \( \sim 15'' \).
It appears nearly circular as projected on the sky, with brightened limbs enhanced toward the southeast. The appearance is consistent with the previously obtained MIPSGAL image at 24 $\mu$m (Carey et al. 2009). Based on its appearance, we treat the nebula as a thin, hollow shell whose far-IR spectrum is due to equilibrium thermal emission from dust grains all at the same distance from the star. This type of shell can result, for example, when a post-red supergiant (post-RSG) star has developed a fast wind during an LBV phase, which sweeps up gas and dust lost during the previous RSG phase or by a previously ejected LBV shell that is swept up by the post-eruption wind (Smith 2014).

### 2.3. Imaging of HD 168625

The FORCAST images of HD 168625 are shown in Figure 4. The nebula is clearly resolved, with a partially complete ring structure that has two peaks almost symmetric around the star. We concur with Meixner et al. (1999) and O’Hara et al. (2003) in their interpretation of these two peaks as limb-brightened peaks of a torus of dust with a radius of $\sim 10''$. The appearance is consistent with previously obtained images at 8.8, 12.5, and 20.6 $\mu$m from Meixner et al. (1999) and PACS 70 $\mu$m images (Groenewegen et al. 2011). We stress that our SOFIA/FORCAST images do not detect the outer polar rings seen in Spitzer IRAC images (Smith 2007), suggesting that the rings must be cold and below the sensitivity limits of SOFIA/FORCAST. The emission detected with the ring morphology in the IRAC band 4 image was probably polycyclic aromatic hydrocarbon (PAH) emission or atomic line emission, not thermal emission from warm dust. Figure 5 shows the temperature map that was derived from stacking the $\lambda F_{\lambda}$ SOFIA/FORCAST 7.7–37.1 $\mu$m images and performing a least-squares fit of the dust temperature, $T_d$, using the best-fit modified blackbody of the SED (i.e., $B_{\lambda}(T_d) \cdot \lambda^{0.33}$) at each pixel location. The images were centered relative to one another by comparing the locations of the limb brightness peaks, and the 7.7–33.6 $\mu$m images were convolved with a 2D Gaussian kernel with an FWHM of 3$''$5 to match the resolution of the 34.8 and 37.1 $\mu$m images. Our temperature map shows a large gradient in dust temperatures with inner torus temperatures of $\sim 180$ K and outer temperatures of $\sim 80$ K, which is in agreement with the estimate of 170 $\pm$ 40 K obtained from our least-squares fit to the IR excess but is slightly higher than the equilibrium temperature estimates made by Pasquali et al. (2002; 113 K), Robberto & Herbst (1998; 135 K), and O’Hara et al. (2003; 130 K). The inaccuracies of this temperature map are due in large part to the fact that the method used to create it assumes that emission is purely thermal and that the dust shell is in thermal equilibrium. As noted previously, much of the 8.8–12.5 $\mu$m flux arises from transient, nonequilibrium emission from PAH grains. Therefore, using images at these wavelengths to derive quantitative conclusions from the temperature map has some limitations; however, we can interpret the maps qualitatively as discussed in Section 4.

### 2.4. IR Reddening

The mid-IR photometry (5–40 $\mu$m) must be dereddened for comparison with the 2-Dust model SED outputs, or conversely, the 2-Dust SEDs must be reddened, as we have done. We used the Fritz et al. (2011) extinction law as it utilizes the most recent near-IR (1–2.4 $\mu$m) observations of the galactic center. We extend the law longward of 24 $\mu$m by adopting the Draine (2003) interstellar extinction curve defined in
Figure 4. Observed SOFIA/FORCAST image (left) and 2-Dust model image (right) of HD 168625 at (a) 7.7 μm, (b) 11.1 μm, (c) 19.7 μm, (d) 25.3 μm, (e) 31.5 μm, (f) 33.6 μm, (g) 34.8 μm, and (h) 37.1 μm with north up and east to the left. The models have been scaled to the same total flux as the observed image and convolved with a Gaussian with FWHM equal to the matching PSF of the SOFIA/FORCAST image (inset white circle). In the observed SOFIA/FORCAST images, the contours are spaced at 1σ, 2σ, and 3σ intervals above the background noise. In the 2-Dust model, the contours are spaced at 20% intervals of the peak intensity. The central star is not included in the model.
Figure 10 of that paper, as was done by Lau et al. (2013). We scaled the $A_K$ of the Fritz et al. (2011) extinction law based on the distance to the objects. We accomplished this by utilizing the 3D Milky Way dust map published by Green et al. (2015) to estimate the extinction. We then converted from extinction to reddening by assuming $A_K = 0.320 \times E(B-V)$, as calculated.
by Yuan et al. (2013) for a 7000 K source spectrum at $E(B-V) = 0.4$ mag, using the Cardelli et al. (1989) reddening law and assuming $R_V = 3.1$.

As mentioned in Section 1, the distance to MN 90 is unknown. In the absence of further information about the star beyond the cataloged 1.2–8 μm photometry, we consider the
implications of assuming that MN 90 is an LBV. We assume a luminosity of $L_\star = 3 \times 10^5 L_\odot$, at the lower end of luminosities for LBVs in their quiescent state between outbursts (see, e.g., Figure 1 of Smith et al. 2004). This luminosity corresponds to $T_\star \approx 14,000$ K. For dust grains with emissivity $Q_\lambda \propto \lambda^{-\beta}$, the radius $r_d$ of the shell may be
computed with

\[ r_d^2 = \frac{L_*}{16\pi\sigma T_d^4} \left( \frac{T_d}{T_{eq}} \right)^\beta, \]

where \( T_d \) is the grains’ equilibrium temperature. Substituting the assumed values for the star and the fitted \( T_d = 59 \) K obtained using \( \beta = 0.76 \) yields \( r_d = 0.47 \) pc. For the shell’s observed angular radius of 20” this places MN 90 at a distance of 4.8 kpc. At this distance, we estimate a reddening of \( A_K = 0.52 \) for MN 90.

The Gaia DR2 (Gaia Collaboration et al. 2018) distance to HD 168625 is 1.61 ± 0.17 kpc or 1.55 kpc using the Bayesian-inferred distance from (Bailer-Jones et al. 2018). We adopt a distance of 1.55 kpc for HD 168625 and estimate a reddening of \( A_K = 0.32 \) for HD 168625. Note that any visual wavelength values are subject to considerable uncertainty; as Fritz et al. (2011) point out, there are several possible extrapolations from their anchor region around Brackett-γ (2.166 μm) into the visual.

3. Radiative Transfer Modeling

3.1. 2-Dust Introduction

We utilize the the axisymmetric radiative transfer code 2-Dust (Ueta & Meixner 2003) to estimate the dust mass and dust shell morphology of MN 90 and HD 168625. The code solves the equation of radiative transfer following the principle of long characteristic (i.e., traces the radiation hitting the dust grain from anywhere in the shell including the star and other dust radiation) in a 2D polar grid, while considering a 3D radiation field at each grid point. The dust opacities are calculated using Mie theory from a user-given size distribution and optical constants of the dust grains. It can be used to model a variety of axisymmetric astronomical dust systems. The dust distribution is expressed analytically as:

\[
\rho(r, \theta) = \rho_{\text{min}} \left( \frac{r}{r_{\text{min}}} \right)^{\beta(1+c \sin^2 \theta)} \exp[-(r/r_{sw})^b]/\exp[-(r_{\text{min}}/r_{sw})^b] \times \{1 + A(1 - \cos \theta)^F \}
\]

\[
\exp[-(r/r_{sw})^b]/\exp[-(r_{\text{min}}/r_{sw})^b] \],
\]

where \( r \) is the radius within the limits of \( r_{\text{min}} \) and \( r_{\text{max}} \), \( r_{sw} \) is the boundary between the spherical AGB wind and the axisymmetric superwind, \( \theta \) is the latitude, and \( \rho_{\text{min}} \) is the dust mass density on the equatorial axis at the inner edge of the envelope. The letters \( A-F \) are input parameters that define the geometry of the dust density profile. The parameter \( A \) changes the overall axisymmetric structure to the shell, which can be made disk-like or toroidal by the parameter \( F \). The parameter \( B \) determines the radial fall-off of the profile and can be a function of the latitudinal angle, \( \theta \), through the parameter \( C \). These parameters determine the toroidal structure of the innermost region of the shell, which is considered to be caused by an axisymmetric superwind at the end of the AGB phase. The mid-region of the shell assumes a somewhat spheroidal dust distribution reflecting the transition of mass-loss geometry from spherical to axial symmetry during the course of the AGB mass-loss history. The parameters \( D \) and \( E \) control the abruptness of the transition in the shell: small values correspond to a slow transition and large values correspond to an abrupt transition. We used a Mathis et al. (1977) power-law grain size distribution:

\[ n(a) = a^{-3.5}, \quad a_{\text{min}} < a < a_{\text{max}}, \]

where \( a_{\text{min}} \) is the minimum grain size and \( a_{\text{max}} \) is the maximum grain size as specified by inputs. Because 2-Dust is axisymmetric, it is not possible to create dust shells with different size parameters in different lobes of the nebula. A more extensive
3.2. Input Parameters

O’Hara et al. (2003) previously analyzed the morphology and parameters for the circumstellar dust around HD 168625 using 2-Dust; therefore, we adopt their parameters as initial values for our model.

Previous mid-IR spectra of HD 168625 by Skinner (1997) indicate the presence of silicates in the dust shell of HD 168625 and previous studies of the dust shells surrounding the LBVs Wra 751 and AG Car indicate that amorphous silicates are the dominant species (Voors et al. 2000). Observations of HD 168625 by Volk & Cohen (1989), Skinner (1997), and Umana et al. (2010) have identified PAHs, which is evident in the IRAS LRS spectra and suggests the possible presence of carbonaceous grains as well. There is also evidence of crystalline forsterite grains being present (Blommaert et al. 2014), which may contribute to the emission seen at ~11 and 19 μm in the IRAS LRS. Therefore, we considered a complex dust distribution model composed of amorphous olivine (MgFeSiO₄; Dorschner et al. 1995), crystalline forsterite (Mg₂SiO₄; Servoin & Priou 1973; Scott & Duley 1996), and amorphous carbon (Rouleau & Martin 1991). However, because 2-Dust cannot account for transiently heated very small dust grains or PAH emission, we ignore fitting the 2-Dust model to the 8-15 μm region.

Most estimates of the effective temperature of the central star of HD 168625 are between 12,000 and 15,000 K (Nota et al. 1996; O’Hara et al. 2003; Mahy et al. 2016), and may vary by a few thousand degrees. The temperature and radius of the star have been adjusted to roughly match the observed SED. However, since the data points are taken by many observers over several decades, we cannot model HD 168625 at any single epoch. The inner radius of the dust shell is well constrained by these mid-IR images to be 8''5 or 0.06 pc at a distance of 1.55 kpc.

As previously mentioned, little is known about MN90 and the central star. We use the SOFIA/FORCAST 37.1 μm image to constrain the angular size of r_min to a value of 20'' or 0.47 pc at a distance of 4.8 kpc. We started with a stellar temperature of 16,000 K and radius 100 Rₒ. Like HD 168625, the temperature and radius of the star have been adjusted to roughly match the observed SED and we used a single species dust distribution of amorphous silicates.

3.3. Model Results

We ran approximately 150 models to obtain the best fit to the SED and SOFIA/FORCAST images of both stars. When available, stellar and dust parameters were taken from previous observations in the literature. We started our modeling by fitting the stellar parameters Tₑ and Rₑ. The mid-IR images constrain the inclination angle (θₑ), inner radius of the dust shell (r_min), and dust density function parameters A-F. We then fit the mass fraction of the mineral species, minimum (a_min) and maximum (a_max) grain sizes, and optical depth at 37.1 μm (τ_{37.1 μm}). We constrained the maximum and minimum grain sizes to be between 0.001 and 2.0 μm. The best-fit model was determined by eye. The best-fit SEDs of MN 90 and HD 168625 are shown in Figures 1 and 2. Input dust distribution parameters for both stars are given in Table 3. Input and derived stellar and dust parameters for the best-fit models of MN 90 are given in Table 4. Input and derived stellar parameters for the best-fit model of HD 168625 are given in Table 5 with the dust parameters summarized in Table 6.

The model SED for MN 90 fits the data well in the wavelength range λ ≥ 8 μm. The discrepancy at shorter wavelengths may be due to the choice of the anchor region for the reddening as discussed in Section 2.4, an underestimate in the distance, or incorrect stellar parameters. Our model image of MN 90 compares well with the FORCAST 37.1 μm image except for the northwest edge of the shell, which appears brighter in the FORCAST image suggesting that the shell is slightly asymmetric. Overall, however, the morphology of the dust shell is well modeled as a symmetric sphere. We found the best-fit density distribution had an amorphous silicate shell extending from r_min = 0.31 pc to 3 r_min = 0.92 pc. The grain size distribution suggests that the silicates have grain sizes between 0.1 and 0.5 μm. Our model gives a dust mass of

| Parameter | MN 90 | HD 168625 |
|-----------|-------|-----------|
| A         | 1     | 30        |
| B         | 2     | 2         |
| C         | 2.5   | 4         |
| D         | 0     | 6         |
| E         | 0     | 3         |
| F         | 0     | 4         |
| θₑ        | 0°    | 55°       |
| τ_{37.1 μm at Equator} | 6 × 10^{-4} | 3.3 × 10^{-3} |

| Parameter | Input | Derived |
|-----------|-------|---------|
| Lₑ × d ≥ 9.3 × 10^4 Lₒ | 6.000 K |
| Rₑ × d ≥ 85 Rₒ | 4.8 kpc |
| ISM A_k | 0.52 |
| r_min ≤ d | 0.35 pc |
| r_max ≥ d | 1.05 pc |
| r_avg ≥ d | 0.52 pc |
| a_min | 0.1 μm |
| a_max | 0.5 μm |
| Vₘ₉₉ | 50 km s⁻¹ |
| Amorphous Silicates | 100% |

Notes.

a Typical for LBVs (Nota et al. 1995).
b MgFeSiO₄ (Dorschner et al. 1995).
c Timescale for mass loss on the AGB.
perpendicular to the plane of the torus, which is consistent with a unified model of LBV nebulae proposed by Nota et al. (1995).

4. Discussion

As previously mentioned in Section 3.2, crystalline forsterite has been detected around HD 168625. This indicates that at least some of the circumstellar material, probably that confined to the torus, has undergone annealing and suggests that the circumstellar environment is similar to that of lower mass progenitors, i.e., PPNs. We should point out that our model for HD 168625 included moderately sized grains (0.1–1.0 μm), slightly larger than the model found by O’Hara et al. (2003; 0.001–1.0 μm), which points to the nebula being relatively young and unprocessed. Aside from the similarities in morphology between PPN and LBVs, a key difference may be the duration of mass loss. Far-IR images at 55 μm of HD 168625 by O’Hara et al. (2003) suggests that the outer dust shell is no more than five times the inner radius. Whereas, for the Egg Nebula, a well-studied PPN, 180 μm images suggest that the outer shell is a few hundred times larger than the inner radius (Speck et al. 2000). The mass-loss shells of LBVs appear to be more compressed than for PPNs, suggesting that the mass loss occurred in a more short-lived (<10^5 year) phase compared with PPNs (~10^5 years).

4.1. MN 90

The morphology of MN 90 lacks a large equator-to-pole mass distribution like most LBVs and is nearly spherical, similar to V4998 Sgr (Lau et al. 2014). The total mass (gas plus dust) lost by the star and the rate of mass loss are estimated to be about 3.2 ± 0.1 M_☉ and (7.3 ± 0.4) × 10^{-6} M_☉ yr^{-1} × (v_{exp}/50 km s^{-1}).

The model SED for HD 168625 fits the data well in most of the wavelength range except for 8–15 μm as discussed in Section 3.2. We confirm the dust distribution model of O’Hara et al. (2003) with only minor differences in the stellar temperature, radius, and grain size distribution. The morphology of the dust is found to be a torus with an equator-to-pole density ratio of 30, an elliptical midshell, and an inclination angle of 55° with the plane of the sky. Our model images compare well with the FORCAST observations except for the gap in the northern rim of the 7.7 μm emission and the gap in the southern rim of the 19.7, 25.3, 31.5, and 33.6 μm emission which may indicate a different composition, azimuthal asymmetry in the dust density distribution around the ring, or the lack of large dust grains in this region. This supports the suggestion that the dust shell may include small, transiently heated dust grains that are not at thermal equilibrium and are not accounted for in these models. The grain size distribution suggests that there are likely only small, transiently heated dust grains in the circumstellar environment. Our model gives a dust mass of (2.5 ± 0.1) × 10^{-3} M_☉ and a dust mass-loss rate of (3.2 ± 0.2) × 10^{-7} M_☉ yr^{-1}. If we rescale the dust mass estimates of O’Hara et al. (2003) using the Gaia DR2 distance, their dust mass changes to (7.7 ± 0.3) × 10^{-3} M_☉ at a mass-loss rate of (6.7 ± 0.3) × 10^{-8} M_☉ yr^{-1}. The discrepancy can be attributed to both the larger grain size distribution and complex dust distribution models, which results in a larger optical depth in our model and a lower dust mass estimate. Our estimate is likely an underestimate of the mass because we are only looking at material in the equator, ~10%–20% of the solid angle of the entire nebula. The bipolar nebula seen in Spitzer images suggests that the circumstellar material at higher latitudes was ejected with higher speed, and therefore it is farther from the star and cooler, which went undetected in the SOFIA imaging that only detects the inner torus. The model suggests that HD 168625 lost mass in a torus-shaped outburst, which has been suggested for all LBVs by Hutsemekers et al. (1994). The current fast wind of the LBV has probably interacted with this torus, creating an elliptical bubble

### Table 5: HD 168625 2-Dust Input and Derived Parameters

| Input |  |
|-------|------|
| L_d \times d | 4.5 \times 10^7 L_☉ |
| T_d | 14500 K |
| R_d \times d | 65 R_☉ |
| d | 1.55 kpc |
| ISM A_K | 0.32 |
| r_{min} \times d | 0.06 pc |
| r_{max} \times d | 0.23 pc |
| r_{m} \times d | 0.20 pc |
| v_{exp} | 19 km s^{-1} |

| Derived |  |
|--------|------|
| M_{dust} \times d^2 | (2.5 \pm 0.1) \times 10^{-3} M_☉ |
| M_{dust} \times d | (3.2 \pm 0.2) \times 10^{-7} M_☉ yr^{-1} |
| \tau_{AGB} | 1.5 \times 10^3 yr |

Notes.

a Pasqualei et al. (2002).
b Timescale for mass loss on the AGB.
Table 6
Dust Properties for Best-fit 2-Dust Model of HD 168625

| Dust Species | Composition | Structure | Mass Fraction | Density | Grain Size | References               |
|--------------|-------------|-----------|---------------|----------|------------|--------------------------|
| Olivine      | MgFeSiO$_4$ | Amorphous | 60%           | 3.71     | 0.001–1.0  | Dorschner et al. (1995)  |
| Forsterite   | Mg$_2$SiO$_4$ | Crystalline | 25%          | 3.22     | 0.500–2.0  | Servoin & Pirou (1973), Scott & Duley (1996) |
| Carbon       | BE sample   | Amorphous | 15%           | 1.44     | 0.001–1.0  | Rouleau & Martin (1991)  |

4.2. HD 168625

The temperature map shows a higher temperature on the southern edge of the dust shell, ~180 K, and a much lower temperature on the northern edge, ~80 K. This same temperature variation was found by O’Hara et al. (2003). O’Hara et al. (2003) suggest that one possible explanation for the different temperatures may be that the grain size distribution varies with respect to position in the nebula. Because smaller grains tend to be warmer than larger grains, this would suggest that the smallest grains are in the southern shell with progressively larger grains toward the northern shell. Pasquali et al. (2002) interpret these distinctive optical morphologies as a variation in the gas-to-dust mass ratio with respect to position in the nebula (i.e., it is higher in the south).

The smaller dust power-law emissivity ($\beta = -0.33$) we have measured for HD 168625 compared to the value used by Robberto & Herbst (1998; $\beta = 1.2$) is likely due to the fact that the circumstellar dust exhibits a large temperature variation (see Figure 5) and emission from small, transiently heated PAH grains (see IRAS LRS in Figure 2). It is not realistic to model the dust as a single temperature—a temperature gradient would be more physically motivated—but in order to compare with previously measured dust temperatures of HD 168625 and to minimize the number of free parameters we only use a single modified blackbody.

Mahy et al. (2016) used Herschel/PACS spectroscopy and CNO abundances to estimate an initial mass of 28–33 $M_\odot$ for HD 168625 and propose that the star lost its mass during or just after the BSG phase and has not yet reached the red supergiant quiescent state, and a distance of 1.55 kpc. Using our dust mass estimate of $1.5 \pm 0.1) \times 10^{-4} M_\odot$ yr$^{-1}$. Dividing our value for $r_{\text{min}} = 0.06$ pc by the nebular expansion velocity measured by Pasquali et al. (2002) gives an expansion time of $\approx 2800$ year, and using our value of $r_{\text{max}} = 0.23$ pc, the mass loss lasted for $\approx 1 \times 10^4$ year.

5. Conclusion

Our SOFIA/FORCAST image at 37.1 $\mu$m of MN 90 shows a limb-brightened, spherical dust shell surrounding the central star. A least-squares fit of a $B_{\lambda} (T_d)$ curve with emissivity $Q_{\lambda} \propto \lambda^{-0.76}$ to the SED of MN 90 yields a dust temperature of 59 ± 10 K, with the peak of the emission at 42.7 $\mu$m. Our 2-Dust model supports the idea that the dust resides in a thin, spherical dust shell and estimates that MN 90 lost $(3.2 \pm 0.1) \times 10^{-7} M_\odot$ of dust in a massive stellar wind with a mass-loss rate of $(7.3 \pm 0.4) \times 10^{-6} M_\odot$ yr$^{-1}$ ($v_{\text{exp}} / 50$ km s$^{-1}$). Using the canonical gas-to-dust mass ratio of 100, we estimate a total mass loss of $3.2 \pm 0.1 M_\odot$ for MN 90. These 2-Dust estimates assume that MN 90 has a luminosity of $9.3 \times 10^4 L_\odot$ at the lower end of luminosities of LBVs in their quiescent state, and a distance of 4.8 kpc. Our 2-Dust model of MN 90 has good agreement with observations if we assume very small, transiently heated silicate grains.

Our SOFIA/FORCAST images between 7.7 and 37.1 $\mu$m of HD 168625 complement previously obtained mid-IR imaging. The dust temperature map that we derive from our observations shows a temperature variation between the northern and southern shells, suggesting different grain size distributions between the two shells. A least-squares fit of a $B_{\lambda} (T_d)$ curve with emissivity $Q_{\lambda} \propto \lambda^{-0.33}$ to the SED of HD 168625 yields an estimated dust temperature of 170 ± 40 K, with the peak of the emission at 18.3 $\mu$m. Our detailed radiative transfer model using 2-Dust supports the claim that the dust resides in a thin, axisymmetric equatorial torus and estimates that HD 168625 lost $(2.5 \pm 0.1) \times 10^{-3} M_\odot$ of dust in a massive stellar wind with a mass-loss rate of $(3.2 \pm 0.2) \times 10^{-7} M_\odot$ yr$^{-1}$. These 2-Dust estimates assume that HD 168625 has a luminosity of $4.5 \times 10^4 L_\odot$ at the lower end of luminosities of LBVs in their quiescent state, and a distance of 1.55 kpc.

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Facility: SOFIA (FORCAST).

Software: 2-Dust.
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