Dispersion-cancelled biological imaging with quantum-inspired interferometry

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Quantum information science promises transformative impact over a range of key technologies in computing, communication, and sensing. A prominent example uses entangled photons to overcome the resolution-degrading effects of dispersion in the medical-imaging technology, optical coherence tomography. The quantum solution introduces new challenges: inherently low signal and artifacts, additional unwanted signal features. It has recently been shown that entanglement is not a requirement for automatic dispersion cancellation. Such classical techniques could solve the low-signal problem, however they all still suffer from artifacts. Here, we introduce a method of chirped-pulse interferometry based on shaped laser pulses, and use it to produce artifact-free, high-resolution, dispersion-cancelled images of the internal structure of a biological sample. Our work fulfills one of the promises of quantum technologies: automatic-dispersion-cancellation interferometry in biomedical imaging. It also shows how subtle differences between a quantum technique and its classical analogue may have unforeseen, yet beneficial, consequences.

Quantum information science promises powerful and unconventional capabilities across a broad range of technologies. An important example relates to the imaging technology, optical coherence tomography (OCT). OCT can noninvasively reconstruct the 3-dimensional structure of tissue with micron resolution; it is emerging as an important clinical tool with diverse medical applications. OCT can diagnose retinal diseases such as glaucoma, analyze atherosclerotic tissues within arteries, and detect early-stage cancerous lesions in breast tissue. In addition, OCT has found application in precision laser machining. Since OCT relies on low-coherence interferometry, its axial resolution is limited by the coherence length of the light, inversely proportional to the bandwidth. The coherence length determines ultimate resolution, however, material dispersion can limit the practical one.

Fundamental studies in quantum optics showed that interference with energy-time entangled photon pairs exhibits inherent robustness against unbalanced dispersion. Even-order effects of dispersion, including the dominant group-velocity dispersion, are automatically cancelled, effectively solving the dispersion problem. This dispersion cancellation is automatic since one does not need to precisely measure and compensate the dispersion. When energy-time entanglement is strong, but not perfect, the effect is more accurately described as automatic even-order dispersion reduction since the dispersion is dramatically reduced, not cancelled. OCT based on entangled-photon interferometry was proposed to harness automatic dispersion cancellation. This quantum-optical coherence tomography (QOCT) has two significant barriers to practical implementation. Firstly, the reliance on producing and resolving individual photon pairs places stringent limits on the QOCT signal using state-of-the-art systems. Secondly, in samples with multiple interfaces, QOCT produces a signal for each interface and an additional, artifact feature for each unique pair of interfaces; the number of artifacts grows quadratically with the number of interfaces, cluttering the image of complex samples. QOCT was first used to perform an axial scan of a coverslip and later applied to measure the surface topography of a gold-coated onion sample. The gold coating was essential to increase reflectivity but rendered the technique impractical for in vivo applications; furthermore, it prevented imaging the sample’s internal structure, which is one of the main benefits of OCT and necessary for most medical applications.

Recently, several different approaches have shown that dispersion cancellation does not require entanglement, but can also be observed in classical systems. While all of these methods could, in principle, solve the low-signal problem of QOCT, each suffers from unwanted artifacts. Here, we focus on one of these techniques,
chirped-pulse interferometry (CPI). A method for identifying artifacts in CPI has been demonstrated, but it requires multiple axial scans of a sample and is thus inherently slow\(^\text{28}\).

In the present work, we describe and demonstrate a new method for CPI using a single beam of shaped laser pulses. Our method produces background-free, dispersion-cancelled signals, completely free of artifacts without the need for multiple scans. We apply this technique to image a biological sample, demonstrating dispersion cancellation and observing the sample’s internal structure. CPI overcomes both limitations of QOCT while retaining its advantages, demonstrating its potential for future practical application.

Results

Theoretical description. CPI uses classical light with strong frequency anti-correlations. To create these anti-correlations, we constructed a 4-F pulse shaper with a spatial light modulator (SLM)\(^\text{20,21}\). In CPI, this method has distinct advantages over pulse-stretching techniques with bulk optics\(^\text{22,23}\), including: straightforward optimization of the chirp parameter\(^8\), better stability and efficiency, and more complex pulse shapes. We apply a frequency-dependent phase shift to the laser pulses, \(\phi(\omega) = -A(\omega - \omega_0)(\omega - \omega_0)\), where \(A\) is a positive constant. The absolute value distinguishes this from the quadratic phase leading to linear chirp: \(\phi(\omega)\) applies a linear chirp to red-shifted frequencies \((\omega < \omega_0)\) and an equal, opposite chirp (antichirp) to blue-shifted frequencies \((\omega > \omega_0)\). The resulting pulse has frequency \(\omega_0\) at its lagging edge, and instantaneous frequencies in the preceding part of the pulse obey the function \(\omega(t) = \omega_0 + t/2A\). These are the frequency anti-correlations needed for CPI. We refer to this as a Blue-Antichirped-Red-Chirped (BARC) pulse.

CPI can be understood by considering the schematic in Figure 1a. Light in the upper arm of the interferometer travels through a dispersive material of length \(L\) as well as a distance \(L_1 - L\) through free space; light in the lower arm travels a distance \(L_2\) through free space. The dispersive material in the upper arm has a wavevector of light that can be expanded about frequency \(\omega_0\) as \(k(\omega) = k(\omega_0) + \alpha(\omega - \omega_0) + \beta(\omega - \omega_0)^2 + \ldots\), where \(\alpha\) and \(\beta\) describe the group delay and group velocity dispersion, respectively. At any time, two laser beams with frequencies \(\omega_0 + \Delta\) and \(\omega_0 - \Delta\) enter the interferometer with corresponding amplitudes \(E(\Delta)\) and \(E(-\Delta)\). After travelling through the interferometer they overlap at the nonlinear crystal for sum-frequency generation (SFG). Two paths produce SFG with frequency \(\omega_0\) either blue-shifted light travels the upper arm and red-shifted light travels the lower arm, or vice versa. The amplitudes for these two paths interfere to give a signal \(S(\Delta, \tau) = |E(\Delta)E(-\Delta)|^2 (1 + \cos [\phi_+(\Delta, \tau) - \phi_-(\Delta, \tau)])\), where \(\tau = (L_2 - L_1 + L)/c\) is the time delay between the two paths\(^{18}\). Second order in the wave-vector and ignoring a global phase, the respective phases of the two paths are, \(\phi_\pm(\Delta, \tau) = L(T\pm \Delta L)\). The final signal results from integrating \(\Delta\) over the pulse bandwidth, forming a peak at \(\tau = \Delta L/2\). Since unbalanced dispersion contributes the same phase \(\beta^{\Delta L}\) to each path, the effect cancels out of the final signal; this is automatic dispersion-cancellation. With imperfect anti-correlations, dispersion cancellation persists if the unbalanced dispersion is much less than the chirp parameter, \(A\) (see ref. 8).

Ideally, each interference signal would correspond to an interface in the sample. However, in both QOCT\(^\text{19}\) and CPI\(^\text{20}\) an additional artifact signal appears halfway between the signals arising from each pair of interfaces. In complex samples, artifacts can outnumber the features from real interfaces, seriously impeding reconstruction and interpretation. The origin of the artifacts in these two techniques are subtly, but importantly different (see Supplementary Fig. S1 online). Artifacts in CPI are a result of interference in the SFG light at frequencies blue-shifted or red-shifted from the operating frequency, \(2\omega_0\), by an amount \(\Delta \omega = \Delta \tau/(4\Delta\lambda)\), where \(\Delta\tau\) is the time-delay difference between the two sample interfaces. Spectral filtering of the SFG can remove all artifacts arising from pairs of interfaces separated by more than some minimum delay. The analogous method of artifact removal in QOCT requires coincidence detection with tens of femtoseconds time-resolution, which is extremely difficult in practice.

![Figure 1](https://www.nature.com/scientificreports/)
Experimental setup and characterization. Our experimental setup is shown in Figure 1b. We used this system to image a stack of two microscope coverglass slips (Figure 1c) and an onion (Figure 1d). First, we focus on the coverglass sample to benchmark our system performance. We measure the SFG power as a function of time delay, \( r \), with two types of pulses, a transform-limited (TL) pulse and the BARC pulse. Using the TL pulse is equivalent to OCT with background-free autocorrelation\(^{15}\), which does not suffer from artifacts but is not dispersion cancelling. In order to remove artifacts from signals acquired with BARC pulses, the SFG signal is sent through a 0.35-nm-bandwidth filter. See Methods for more details.

The data measured using TL and BARC pulses are shown in Figures 2a and b, respectively. Black (red) lines show data without (with) unbalanced dispersion from 3-mm BK7 in the sample arm, where the light passes twice through the glass. The left-most four peaks correspond to the front and back surfaces of the first and second coverglass pieces. The average delay between the first (second) two peaks is 248 ± 4 \( \mu m \) (236 ± 4 \( \mu m \)). Dividing by the group index \( n_g = 1.517 \) of the coverglass gives thicknesses of 163 \( \mu m \) and 156 \( \mu m \) for the two slides, in good agreement with 164 ± 3 \( \mu m \) and 157 ± 3 \( \mu m \) measured with a caliper. We subtracted a constant 1.6 mm from the delay-arm motor position in the unbalanced-dispersion data to compensate for the group delay from the additional glass so corresponding peaks could be overlaid for comparison.

Figures 2a and b show that no additional artifact features arise going from a TL to a BARC pulse. In the online Supplementary Information, we show the maximum layer separation giving rise to artifacts is 3 \( \mu m \), narrower than the peak widths, 4.2 \( \mu m \). As expected, any resolvable artifacts are filtered out of our signal.

The average signal peak width for the TL pulses is 3.6 ± 0.2 \( \mu m \) (FWHM) which broadened by 106% to 7.4 ± 0.6 \( \mu m \) by the dispersion. Uncertainties represent the standard deviations of the five peak widths. In contrast, the BARC-pulse produced average signal widths of 4.2 ± 0.1 \( \mu m \) that broadened by only 7% to 4.5 ± 0.2 \( \mu m \), demonstrating dispersion cancellation. The measured peak widths for the TL and BARC pulses are in good agreement with the theoretical calculations of 3.4 \( \mu m \) and 4.1 \( \mu m \), respectively, using the 60 nm acceptance bandwidth of our system. The peak width of the BARC-pulse signal is broadened compared to the TL pulses as a result of the narrow filtering of the SFG; if a broader bandwidth was measured instead, the widths would become equal, but artifacts can reappear. The dispersion cancellation observed cannot be explained by the slightly broader BARC-pulse signal in the balanced dispersion case. If one used a TL pulse yielding a 4.2 \( \mu m \) peak width in the absence of dispersion, equal to the width to our BARC-pulse signal, we calculate that two passes through 3-mm BK7 glass would broaden the signal to 5.8 \( \mu m \), a 38% increase. Our BARC-pulse signal is broadened by 7%, thus the dispersion cancellation is significant even when compared with this conservative benchmark.

**Dispersion-cancelled biological imaging.** We prepared a sample of onion as depicted in Figure 1d and took a set of axial (z) scans, moving the sample in the \( y \)-direction between scans. The data are displayed in Figure 3, where the four panels a, b, d, and e show cases with and without dispersion (3-mm BK7) for both TL and BARC pulses. The vertical axes are the delay-arm motor positions and the horizontal axes show the transverse \( y \)-positions. The images show the cellular structure of the onion deep into the sample and are artifact-free. Beside each image, we show a single axial scan taken at the \( y \)-position marked by the red line in each plot. The TL-pulse signal peaks are dramatically broadened when unbalanced dispersion is added, but the BARC-pulse peak widths are unchanged, directly demonstrating automatic dispersion cancellation in our image. In order to compare the effect of dispersion over the entire images produced by the TL pulses and BARC pulses, we extracted the widths of signal peaks throughout the images and display corresponding histograms in Figures 3c and f. The TL-pulse peaks broadened by 61% from an average of 3.6 ± 0.5 \( \mu m \) to 5.7 ± 1.2 \( \mu m \), where uncertainties are the standard deviations of each distribution. The BARC-pulse peak widths increased by only 4% from 4.2 ± 0.8 \( \mu m \) to 4.3 ± 0.6 \( \mu m \), less than the standard deviation. Hence, dispersion is cancelled throughout the BARC-pulse images.

To further show the capability of our method, we took a set of axial (z) scans over a grid of \( x \)- and \( y \)-positions of a different onion sample prepared in the same manner as before, using the BARC pulses with no unbalanced dispersion. From this data, we extracted 2D cross-sections of the sample shown in Figures 4a–c and the 3D cell wall structure of the top layer of cells is shown in Figure 4d. Thus CPI, with its inherent dispersion cancellation, is suitable for practical 3D imaging of biological samples.

**Discussion**

We have demonstrated dispersion-cancelled, artifact-free, optical-coherence-tomography imaging of a biological sample. For future work, incorporating a nonlinear material with larger nonlinearity
and acceptance bandwidth\(^2\)
will improve the system, increasing acquisition rates and image resolution. Dispersion-cancelled OCT with chirped-pulse interferometry draws upon insights from quantum information science. Exploiting subtle differences in the analogous roles played by different physical parameters between the techniques allowed problems inherent to the quantum scheme to be solved in the classical technology; extraction of artifacts is very hard, or even technologically impossible, in the quantum device, yet becomes straightforward in CPI. Our results remove the technological barriers to dispersion-cancelled biological imaging and underscore the importance of understanding classical analogues to quantum mechanical effects.

Figure 3 | Two-dimensional images of an onion sample. Panel (a) was taken with the TL pulse with no unbalanced dispersion, (b) TL pulse with 3 mm of BK7 in the sample arm for unbalanced dispersion (d) BARC pulse, no dispersion, and (e) BARC pulse with unbalanced dispersion. The colour-bar represents the natural logarithm of the number of counts per delay-arm motor step recorded by the photomultiplier. The internal cellular structure of the onion is visible deep into the sample in all four images and comparing the images we see that no artifacts are introduced by using BARC pulses. A single axial scan at the transverse position indicated by the red vertical line in each image are plotted on a linear scale beside each corresponding image; the labels represent the widths of each peak FWHM in micrometres. The addition of dispersion significantly broadens the TL-pulse peaks while in contrast the BARC-pulse peaks are dispersion cancelled. Peak widths over each entire image are plotted as histograms shown in panels (c) and (f), for the TL and BARC pulses respectively; the black bars are used for no unbalanced dispersion and the red for unbalanced dispersion. The peak widths for the TL pulses broadened by 61% with the addition of dispersion, while those from the BARC pulses broadened only by 4%. Dispersion cancellation is thus achieved over the entire image.

Figure 4 | A three-dimensional image of an onion sample. Using BARC pulses with no unbalanced dispersion, we took a set of axial (z) scans at a grid of x- and y-positions on an onion sample. Panels (a), (b), and (c) show 2D cross-sectional images of our 3D data in the xz, yz, and xy planes depicting the cellular structure. In panel (d), we show a 3D rendering of the surface layer of cells extracted from our data. The grid spacing is 50 \(\mu\)m, and the transparent red planes correspond to the slices shown in panels (a), (b), and (c).
Methods

Pulses from a titanium:sapphire laser (808 nm, 90 nm FWHM) pass through a 4-F pulse shaper incorporating a spatial light modulator (CRi SLM-640-D-VN)

Altepeter, J., Jeffrey, E. & Kwiat, P. Phase-compensated ultra-bright source of pulse shaper (2006). Phys. Rev. A 74, 041601(R) (2006).

Banaszek, K., Rudolph, A. S. & Walmsley, J. A. Blind dispersion compensation for optical coherence tomography. Opt. Commun. 269, 152–155 (2007).

Resch, K. J., Puvanathasan, P., Lundein, J. S., Mitchell, M. W. & Bizheva, K. Classical dispersion-cancellation interferometry. Opt. Express 15, 7977–8804 (2007).

Kaltenbaek, R., Lavoie, J., Biggerstaff, D. N. & Resch, K. J. Quantum-inspired interferometry with chirped laser pulses. Nature Phys. 4, 864–868 (2008).

Le Gouët, J., Venkatraman, D., Wong, F. N. C. & Shapiro, J. H. Experimental realization of phase-cancelled optical coherence tomography. Opt. Lett. 35, 1001–1003 (2010).

Weiner, A. M. Femtosecond pulse shaping using spatial light modulators. Rev. Sci. Instr. 71, 1922–1960 (2000).

Légaré, F. L., Fraser, J. M., Villeneuve, D. M. & Corkum, P. B. Adaptive compression of intense 250-nm-bandwidth laser pulses. Appl. Phys. B 74(Suppl.), S279–S282 (2002).

Martínez, O. E. Matrix Formalism for Pulse Compressors. IEEE J. Quantum Electron. 34, 2530–2536 (1998).

Pessot, M., Main, P. & Mourou, G. 1000 times expansion/compression of optical pulses for chirped pulse amplification. Opt. Commun. 62, 419–421 (1987).

Pe’er, A., Bromberg, Y., Dayan, B., Silberberg, Y. & Friesem, A. Broadband sum-frequency generation as an efficient two-photon detector for optical tomography. Opt. Express 15, 8760–8769 (2007).

Lavoie, J., Kaltenbaek, R. & Resch, K. J. Quantum-optical coherence tomography with classical light. Opt. Express 17, 3818–3825 (2009).

Kaltenbaek, R., Lavoie, J. & Resch, K. J. Classical Analogues of Two-Photon Quantum Interference. Phys. Rev. Lett. 102, 243601 (2009).

Nasr, M. B. et al. Ultrabroadband Biphotons Generated via Chirped Quasi-Phase-Matched Optical Parametric Down-Conversion. Phys. Rev. Lett. 100, 183601 (2008).

Schreiter, K. Optical pulse shaping for chirped pulse interferometry and bio-imaging. M. Sc. Thesis. University of Waterloo, Canada. (2011).