Zwicky Transient Facility and Globular Clusters: the Period-Luminosity and Period-Luminosity-Color Relations for Late-Type Contact Binaries

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ABSTRACT

In this work, we aimed to derive the gri-band period-luminosity (PL) and period-luminosity-color (PLC) relations for late-type contact binaries, for the first time, located in the globular clusters, using the homogeneous light curves collected by the Zwicky Transient Factory (ZTF). We started with 79 contact binaries in 15 globular clusters, and retained 30 contact binaries in 10 globular clusters that have adequate number of data points in the ZTF light curves and unaffected by blending. Magnitudes at mean and maximum light of these contact binaries were determined using a fourth-order Fourier expansion, while extinction corrections were done using the Bayerstar2019 3D reddening map together with adopting the homogeneous distances to their host globular clusters. After removing early-type and “anomaly” contact binaries, our derived gri-band PL and period-Wesenheit (PW) relations exhibit a much larger dispersion with large errors on the fitted coefficients. Nevertheless, the gr-band PL and PW relations based on this small sample of contact binaries in globular clusters were consistent with those based on a larger sample of nearby contact binaries. Good agreements of the PL and PW relations suggested both samples of contact binaries in the local Solar neighborhood and in the distant globular clusters can be combined and used to derive and calibrate the PL, PW and PLC relations. The final derived gr-band PL, PW and PLC relations were much improved than those based on the limited sample of contact binaries in the globular clusters.

1. INTRODUCTION

Contact binaries (CB) are binary systems with two stars overflow their Roche lobes, majority of them have orbital period less than a day. CB include more massive early-type systems and less massive late-type systems – commonly known as W UMa (W Ursae Majoris) type binaries. In this work, we used the term CB to refer for both types, although majority of the CB mentioned in the cited literature are belong to W UMa system. For reviews on CB, see (for example) Smith (1984), Webbink (2003) and Paczyński et al. (2006). In analog to classical pulsating stars (e.g., Cepheids and RR Lyrae), CB also exhibit a period-luminosity (PL) relation or a period-luminosity-color (PLC) relation, albeit the physics behind their PL and PLC relations is different than the classical pulsating stars. Brief theoretical framework on the PL and PLC relations for CB can be found, for example, in Rucinski (1994, 1996, 2004) and Chen et al. (2016), and will not be repeated here. Chen et al. (2016) and more recent work from Chen et al. (2018) demonstrated the PL relations for CB could be used as distance indicators at a level that is competitive to the classical standard candles such as Cepheids.

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Some earlier work on deriving the PL or PLC relations for CB can be found in Rucinski (1974) and Mochnacki (1981, equation 22 in the paper). Since then, a number of papers have been published by Rucinski and co-workers to calibrate the PL and PLC relations for CB in the BV1-bands using parallax measurements, CB in open clusters and a few CB with visual companions (see Rucinski 1994; Rucinski & Duerbeck 1997a,b; Rucinski 1997a, 2006; Mateo & Rucinski 2017). Independently, Eker et al. (2009) improved the calibration of optical PLC relation using 31 systems with most accurate Hipparcos parallaxes by applying the Lutz-Kelker corrections (Lutz & Kelker 1973) and extending the PLC calibration to the near infrared JHK bands. The K-band PL relation was also presented in Muraveva et al. (2014). Later, Chen et al. (2016) derived the JHK-band PL relations using 66 CB in open clusters (42 systems), moving groups (4 systems) and those with accurate parallaxes from Hipparcos (20 systems), as well as the V-band PL relation based on a much larger sample. In Chen et al. (2018), twelve bands PL relations spanning from optical to infrared were derived using a sample of ∼ 183 CB with parallax measurements based on Tycho-Gaia astrometric solution (as part of the Gaia Data Release 1). The calibrated PL or PLC relations presented in these work were mainly based on the late-type W UMa systems. In case of the early-type CB, the J-band PL relation was derived in Chen et al. (2016), while the optical PLC relation was presented in Pawlak (2016) based on 64 early-type CB located in the Large Magellanic Cloud. Using a much larger sample of CB, Jayasinghe et al. (2020) showed that early-type and late-type CB follow a different PL relation. Finally, Sun et al. (2020) divided CB into three sub-classes and derived the mid-infrared W1-band PL relation for each of them.

Besides open clusters and parallax measurements, globular clusters provide a viable and yet independent route to calibrate their PL and PLC relations. CB in globular clusters shared the same distances at which independent and reliable distances of globular clusters from various methods can be found in literature. Majority of the globular clusters are located in high Galactic latitudes, therefore the effect of extinction is tended to be minimal. The CB in globular clusters also provides a consistency check of the PL and PLC relations extending to the old populations and low metallicity environment (e.g. see Rucinski 2000). Since majority of the CB observed by LAMOST have sub-Solar metallicity (Qian et al. 2017), the route of using globular clusters to calibrate the PL and PLC relations might be more appropriate. Even though not numerous, CB indeed could be found in a number of globular clusters. For instance, Li et al. (2010) provided a list of globular clusters containing CB, the number of the CB in the 17 listed globular clusters ranged from 1 to 18 for a total of 230 systems. Other compilations of CB in globular clusters, in the format of NGC/NGB (where NGC and NCB is the total number of globular clusters and CB, respectively), include Hut et al. (1992, 5/15), Rucinski (1995, 3/10), Mateo (1996, 7/24), Rucinski (2000, 14/68)1, and Li et al. (2017, 5/11).

The main goal of our work is to derive the gri-band PL and PLC relations using CB found in the globular clusters. The optical PL or PLC relations derived in the literature mentioned earlier do not include the gri-band, this motivated us to derive such relations using the homogeneous photometric data obtained from the Zwicky Transient Facility (ZTF, Bellm & Kulkarni 2017; Bellm et al. 2019; Graham et al. 2019). Our derived gri-band PL and/or PLC relations can then be applied to the large number of CB observed with the same or similar filters set, for example, those CB observed with the Dark Energy Camera (DECam, Flaugher et al. 2015), discovered in ZTF Data Release 2 (Chen et al. 2020), and the faint CB to be discovered by the Vera C. Rubin Observatory’s Legacy Survey of Space and Time (LSST, Ivezić et al. 2019). In Section 2, we described the selection of globular clusters and the CB within them, as well as the ZTF light curves data for the selected CB. Period refinements for these selected CB were given in Section 3. We then performed light curves fitting using Fourier expansion to derive their magnitudes at mean and maximum light in Section 4. Fitting of the PL and PLC relations will be done in Section 5 and 6, respectively. An example on the application of the derived PL relation will be presented in Section 7, followed by conclusions in Section 8.

2. SAMPLE AND DATA

2.1. Selection of Contact Binaries in Globular Clusters

The samples of CB in globular clusters were obtained from Clement (2017, hereafter the Clement’s Catalog), an updated version of Clement et al. (2001). We first selected globular clusters that are observable with ZTF (δJ2000 > −30°), for those selected globular clusters we searched for variable stars classified as “EW” or “EC” in the Clement Catalog. Those EW or EC binaries marked as foreground or suspected foreground stars in the Clement Catalog were

1 The number of CB should be 68 (as listed in Table 2 of the paper) instead of 86. Also, a fraction of the CB (about 1/3 to half) were foreground or background stars.
Therefore, our final list consists of 79 CB in 15 globular clusters. Positions and periods for CB in M10, M22 and NGC6712 were reduced and calibrated with a dedicated reduction pipeline, as detailed in

| Name  | $\alpha_{2000}$ | $\delta_{2000}$ | $D^b$ | $E(B-V)^{b}$ | [Fe/H] | $N_{CB}$ | $N_{CB}^{ZTF}$ | Reference$^c$ |
|-------|----------------|----------------|-------|--------------|--------|---------|---------------|-------------|
| M4    | 16:23:35.22    | $-26:31:32.7$ | 1.97 $\pm$ 0.04 | 0.35 | $-1.16$ | 19 | 12 | 1,2,3,4,5 |
| M9    | 17:19:11.26    | $-18:30:57.4$ | 8.40 | 0.38 | $-1.77$ | 3 | 3 | 6,7 |
| M12   | 16:47:14.18    | $-01:56:54.7$ | 4.67 $\pm$ 0.21 | 0.19 | $-1.37$ | 3 | 3 | 8,9 |
| M13   | 16:41:41.24    | $+36:27:35.5$ | 6.77 $\pm$ 0.28 | 0.02 | $-1.53$ | 2 | 1 | 10,11 |
| M15   | 21:29:58.33    | $+12:10:01.2$ | 10.22 $\pm$ 0.13 | 0.10 | $-2.37$ | 2 | 2 | 12 |
| M22   | 18:36:23.94    | $-23:54:17.1$ | 3.23 $\pm$ 0.08 | 0.34 | $-1.70$ | 17 | 9 | 13,14,15 |
| M30   | 21:40:22.12    | $-23:10:47.5$ | 8.00 $\pm$ 0.57 | 0.03 | $-2.27$ | 4 | 2 | 16 |
| M71   | 19:53:46.49    | $+18:46:45.1$ | 3.99 $\pm$ 0.20 | 0.25 | $-0.78$ | 9 | 9 | 17 |
| NGC4147 | 12:10:06.30   | $+18:32:33.5$ | 18.20 | 0.02 | $-1.80$ | 5 | 5 | 18 |
| NGC5466 | 14:05:27.29   | $+28:32:04.0$ | 16.90 | 0.00 | $-1.98$ | 2 | 1 | 19 |
| NGC6401 | 17:38:36.60   | $-23:54:34.2$ | 7.70 | 0.72 | $-1.02$ | 6 | 4 | 20 |
| NGC6712 | 18:55:06.04   | $-22:42:05.3$ | 6.95 $\pm$ 0.39 | 0.22 | $-1.36$ | 2 | 2 | 21 |

$^a$ Distance $D$ (in kpc) adopted from Baumgardt et al. (2019).
$^b$ These values were adopted from the Milky Way Globular Clusters Catalog (December 2010 version; Harris 1996, 2010).
$^c$ The number of CB (see text for details).
$^d$ The number of CB that contain at least one ZTF data point in any filters.
$^e$ The references on CB are: (1) Kaluzny et al. (1997); (2) Kaluzny et al. (2013); (3) Nascimbeni et al. (2014); (4) Stetson et al. (2014); (5) Safonova et al. (2016); (6) Clement & Shelton (1996); (7) Arellano Ferro et al. (2013); (8) von Braun et al. (2002); (9) Kaluzny et al. (2015); (10) Pietrukowicz & Kaluzny (2004); (11) Deras et al. (2019); (12) Jönk et al. (2001); (13) Kaluzny & Thompson (2001); (14) Pietrukowicz & Kaluzny (2003); (15) Rozyczka et al. (2017); (16) Pietrukowicz & Kaluzny (2004); (17) Park & Nemec (2000); (18) Lata et al. (2019); (19) Mateo et al. (1990); (20) Sozzi et al. (2016); (21) Deras et al. (2020).

Further removed. After applying the mentioned selection criteria, the preliminary list of CB included 45 EW and 25 EC in 15 globular clusters.

This preliminary list of CB was updated based on new discoveries published in recent years. New CB that were confirmed to be members of globular clusters were added for M4 (Safonova et al. 2016, 1 new CB added), M10 (Rozyczka et al. 2018, 1 new CB added), M12 (Kaluzny et al. 2015, 3 new CB added), M13 (Deras et al. 2019, 1 new CB added), M22 (Rozyczka et al. 2017, 6 new CB added), NGC4147 (Lata et al. 2019, 5 new CB added) and NGC6712 (Deras et al. 2020, 2 new CB added). Positions and periods for CB in M10, M22 and NGC6712 were also updated, whenever available, from Arellano Ferro et al. (2020), Rozyczka et al. (2017) and Deras et al. (2020), respectively. KT-42 in M22 was reclassified as EW variable (Rozyczka et al. 2017) hence it was added to the list. Similarly, CB that turned out not to be a member of the globular clusters or being re-classified as other types of variable stars were removed. These include: V2 in M12 (Kaluzny et al. 2015); KT-01, KT-03, KT-15, KT-39, KT-40 & KT-41 in M22 (Rozyczka et al. 2017); V27, V28 & V29 in NGC6712 (Deras et al. 2020); V97 in M14 (Contreras Peña et al. 2018); and V10 in NGC288 (Lee et al. 2016). Therefore, our final list consists of 79 CB in 15 globular clusters.

2.2. Light Curves from ZTF

ZTF carried out a multi-band time-domain optical surveys on northern sky using the Samuel Oschin 48-inch Schmidt telescope, located at the Palomar Observatory. For more details on ZTF, see Bellin et al. (2019) and Graham et al. (2019), and will not be repeated here. Observing time, hence the data right, of ZTF were divided into partner surveys, public surveys and those reserved for the California Institute of Technology (Caltech). The ZTF imaging data were reduced and calibrated with a dedicated reduction pipeline, as detailed in Masci et al. (2019). ZTF light curves for the CB in our list were extracted, using an 1 arc-second match radius, from the PSF (point spread function) catalogs generated from the dedicated ZTF pipeline. These PSF catalogs include the public and Caltech data from the ZTF Public Data Release 3$^2$ and the ZTF private data spanning from commissioning (October 2017) to 30 September 2020. However, only 53 CB in 12 globular clusters have ZTF light curves data, as summarized in Table 1, and no ZTF light

$^2$ https://www.ztf.caltech.edu/page/dr3
curves data were extracted for CB in M10, M80 and NGC2419. The extracted ZTF light curves data for these 53 CB were provided in Table 2, with 1 to ∼650 data points per ZTF light curves (in either one of the ZTF’s gri filters). We further removed 10 CB (69_K50, 70_K51 & 100_N13 in M4; V3 in M12; KT-08 & KT-33 in M22; P8 & P12 in M71; V43 & V54 in NGC6401) with sum of the data points per light curves in all gri-band that was less than 20, leaving 43 CB in our sample. All of these 43 CB have ZTF light curves data in gr-band, and some (21) of them included additional i-band light curves. For the remaining light curves, we excluded outliers that were deviated by more than ±0.75 mag from the median values of the light curves, because the light curve amplitudes for CB in general would not exceed 1.2 mag (for example, see Rucinski 1998, 2001; Dey et al. 2015; Chen et al. 2018). Therefore, we adopted ±0.75 mag as a conservative cut to remove the outliers.

3. PERIODS REFINEMENT

Since it is well known that CB will undergo period change (e.g., see van’t Veer 1972; Wolf et al. 2000; Rovithis-Livaniou 2006; Pilecki et al. 2007; Lohr et al. 2013), we therefore decided to obtain the orbital periods (P) for our sample of CB from ZTF light curves, and not adopting the published periods reported in the literature.

The Lomb-Scargle (Lomb 1976; Scargle 1982) periodogram is a widely used method to search for periodicity of variable stars, which is based on fitting the unevenly sampled light curve data with a sinusoidal model (for a review on Lomb-Scargle periodogram, see VanderPlas 2018). Because the shape of the CB light curve is near sinusoidal, it is common to apply Lomb-Scargle periodogram to search for their orbital periods. Majority of the codes that implement the Lomb-Scargle periodogram algorithm, however, rely on the light curve data taken in the same filter. An exception is gatspy (VanderPlas & Ivezić 2015; VanderPlas 2016) which can be run on either the single-band or the multi-band light curve data. Given the fact that shapes and amplitudes of the light curve for CB are almost independent of filters and ZTF multi-band observations were not in simultaneous (or near simultaneous), we applied three period search methods on the multi-band light curves for the 43 CB in the sample. The first two methods used the Lomb-Scargle periodogram in a different way, at which the first method constructed an effectively “single-band” light curve by combining the multi-band light curve data, while the second method utilized the multi-band version of the Lomb-Scargle periodogram. The third method is independent of Lomb-Scargle periodogram, at which a non-parametric smoother called the SuperSmother (Reimann 1994) was used to search for periodicity. The SuperSmother algorithm does not rely on the assumption of sinusoidal-like light curve. The three period search methods applied on a given CB are:

- **Method I:** The gr(i)-band light curves were combined after subtracting the median values of each light curves, hereafter referred as the combined light curves. The Lomb-Scargle periodogram, implemented either in astropy (Astropy Collaboration et al. 2013, 2018) or gatspy, was used to search for periods in the range of 0.1 to 2.0 days on the combined light curve, and twice of the best period found was adopted.

- **Method II:** The multi-band Lomb-Scargle periodogram, LombScargleMultiband implemented in gatspy, was run on the gr(i)-band light curves with period range specified in between 0.1 to 2.0 days, and twice of the best period found was adopted.

- **Method III:** The multi-band SuperSmother periodogram, SuperSmotherMultiband implemented in gatspy, was run on the gr(i)-band light curves with period range restricted within 10% of the published period.

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**Table 2. ZTF light curves data for CB in the globular clusters.**

| G.C. | CB Name | ZTF Filter | MJD     | Mag. | Mag Error |
|------|---------|------------|---------|------|-----------|
| M12  | V3      | g          | 58617.4159838 | 19.169 | 0.250     |
| M12  | V3      | g          | 58672.1844329 | 19.027 | 0.334     |
| M12  | V3      | g          | 58715.1481944 | 19.583 | 0.341     |
| M12  | V3      | r          | 58300.3152894 | 18.136 | 0.185     |
| M12  | V3      | r          | 58331.1678009 | 18.270 | 0.346     |

*Note:* Table 2 is published in its entirety in the machine-readable format. A portion is shown here for guidance regarding its form and content.
Table 3. Comparison of periods found with Method I, II and III to the published periods.

| G.C. | Var. Name | Published Period (days) | Method I (days) | Method II (days) | Method III (days) |
|------|-----------|-------------------------|----------------|-----------------|------------------|
| M12  | V6        | 0.256196                | **0.256193**   | 0.278736        | 0.230562         |
| M12  | V8        | 0.435135                | **0.435132**   | 0.435145        | 0.435164         |
| M13  | V57       | 0.285416                | **0.285408**   | **0.285406**    | 0.285408         |
| M15  | V157      | 0.23306                 | **0.246187**   | **0.246194**    | **0.246191**     |
| M15  | V158      | 0.233571                | **0.236162**   | **0.236164**    | **0.236167**     |
| M22  | KT-07     | 0.329797                | **0.329787**   | 0.329787        | 0.331186         |
| M22  | KT-23     | 0.298523                | **0.298527**   | 0.299041        | 0.299041         |
| M22  | KT-43     | 0.22052                 | **0.224590**   | **0.236164**    | **0.236167**     |
| M22  | V118      | 0.280272                | **0.280376**   | 1.965056        | 0.280477         |
| M22  | K44       | 0.263584                | **0.263586**   | **0.244123**    | **0.238292**     |
| M22  | K47       | 0.269875                | **0.269882**   | 0.244124        | 0.244124         |
| M22  | K48       | 0.282694                | **0.285408**   | 0.285408        | 0.285408         |
| M22  | K53       | 0.308448                | **0.310697**   | **0.323251**    | **0.291010**     |
| M22  | K55       | 0.298523                | **0.298527**   | 0.299041        | 0.299041         |
| M22  | V157      | 0.23306                 | **0.246187**   | **0.246194**    | **0.246191**     |
| M22  | V158      | 0.233571                | **0.236162**   | **0.236164**    | **0.236167**     |
\[a\] Range of the searched periods is set to [0.05, 0.40] days.

\[b\] Range of the searched periods is set to [0.05, 0.25] days.

Note—For each CB, the adopted periods from Method I, II and III are marked in boldface.

Results of the periods found with these three methods are listed in Table 3, together with final adopted periods and the published periods. In several CB, we used a smaller period range when applying Method I & II (as indicated in Table 3). The returned periods from these three methods were then used to fold the ZTF light curves and visually inspected. Period that can fold the gr(i)-band light curves closely resembling the CB-like light curve was adopted and marked as boldface in Table 3. As can be seen from Table 3, Method I generally gives the best-fit periods, nevertheless in several cases Method II or III provides a better period to fold the light curves. While visually inspecting these folded light curves, we found that light curves for 13 CB (including all of the CB in M30 and NGC4147, respectively) were seriously affected by blending (such as the light curves were flat or too bright when compared to the published V- or I-band data), therefore they were removed from the sample. For the remaining 30 CB (listed in Table 4), periods found in this work agreed within 1 second or less with the published periods for 19 CB, and another 4 CB the agreements were within 1 minute. The rest of the 7 CB the difference of the periods varied from ~6 minutes to ~4 hours. Figure 1 presents the phased light curves folded with periods used in this work and the published periods for the top 3 CB that have the largest deviations, clearly the periods found in this work can fold the light curves better. Comparisons of the folded light curves with published periods and the periods adopted in this work are presented in the Appendix.

4. LIGHT CURVES FITTING WITH FOURIER EXPANSION

The near sinusoidal shape of the CB’s light curves indicates these light curves can be well represented by a truncated Fourier expansion (Rucinski 1973, 1993; Čoker et al. 2013). Indeed, low-order Fourier expansion has been used to
Figure 1. Comparison of the phased light curves folded with periods found here (top panel in each sub-figures) and the published periods given in the literature (bottom panel in each sub-figures) for the 3 CB with the most discrepant periods. $\Delta P$ is the difference between the period found here and the published period. In each light curves, the blue circles, green squares and red triangles are for the $g$-, $r$- and $i$-band data, respectively. Crosses represent the rejected outliers of the light curves. For a given CB, median values of each light curve in the $gr$-band (and $i$-band if available) were subtracted from the respected light curves before they were combined together. Similar plots for other CB were presented in the Appendix.

separate out CB from other types of eclipsing binaries (mainly the Algol and Beta Lyrae types; for example in Rucinski 1997a,b; Selam 2004; Derekas et al. 2007; Lee et al. 2014; Muraveva et al. 2014; Nedorošić et al. 2015; Yang et al. 2020) or to classify CB against different types of variable stars in time-series surveys (for example, see Pojmanski 2002; Eyer & Blake 2005; Debosscher et al. 2007; Hoffman et al. 2009; Kim et al. 2014; Masi et al. 2014; Jayasinghe et al. 2019). In this work, a 4$^{\text{th}}$-order Fourier expansion (Derekas et al. 2007; Deb & Singh 2011; Dey et al. 2015; Chen et al. 2018) in the following form was adopted to fit the folded ZTF light curves for the CB listed in Table 4:

$$m(\phi) = m_0 + \sum_{j=1}^{4} [a_j \cos(2\pi j \phi) + b_j \sin(2\pi j \phi)],$$  \hspace{1cm} (1)

where $m(\phi)$ are magnitudes, and $\phi$ from 0 to 1 represent the (orbital) phases of the light curves after folded with adopted periods in Section 3. $m_0$, $a_j$ and $b_j$ are the Fourier coefficients to be fitted.

Since equation (1) contains 9 Fourier coefficients, the ZTF $gr(i)$ band light curves with more than 9 data points were fitted with the 4$^{\text{th}}$-order Fourier expansion. However, the fittings would be influenced by how even the data points were distributed on the folded light curves. Figure 2(a) shows an example of a CB with small number of data points in the $g$- and $r$-band light curves, at which the fittings of the 4$^{\text{th}}$-order Fourier expansion were unacceptable due to the presence of a large gap in the folded light curves (as demonstrated with the dashed curves in the plot).

To remedy this problem, for each CB we constructed a template light curve by fitting the 4$^{\text{th}}$-order Fourier expansion to the combined light curve, because the combined light curve has a much larger number of data points per light curve to constrain the fitted Fourier coefficients better. Examples of the the constructed template light curves were shown in the top panels of Figure 2 as solid curves. The template light curve was then shifted vertically with an amount of $\Delta m$ to fit the individual $gr(i)$-band light curves for a given CB by minimizing their error sum of squares (SSE). Lower panel of Figure 2(a) (for M22 KT-43) clearly demonstrated the improvement of using the template light curve to fit the sparsely sampled ZTF light curves (similar improvement can also be seen in the $g$-band light curve of M12 V6). Another advantage of using the template light curve is it can be use to fit light curves with number of data points that was less than 9, as in the case of $i$-band light curve for M12 V6, see Figure 2(b). When the individual $gr(i)$-band light curves were well sampled (with a large number of data points per light curves, such as 200 or more), both of the fitted template light curves and the fitted 4$^{\text{th}}$-order Fourier expansion on the individual $gr(i)$-band light curves were (almost) indistinguishable, as shown in the lower panel of Figure 2(c) (for M71 P2; and the $r$-band light curve of M12 V6).

We compare the fitted light curves between the template light curves and the individual $gr(i)$-band light curves (i.e. the solid and dashed curves in the bottom panels of Figure 2), all fitted with a 4$^{\text{th}}$-order Fourier expansion, by calculating the averaged absolute difference between them. The averaged absolute difference between
the template light curve, $m(\phi)_{\text{template}}$, and the individual $gr(i)$-band light curve, $m(\phi)_{\text{single}}$, is defined as

$$\Delta_{\text{LCF}} = \langle |m(\phi)_{\text{template}} - m(\phi)_{\text{single}}| \rangle,$$

where $m(\phi)$ represents both of the fitted template and single-band light curves based on equation (1) for 1000 phase points ($\phi$) evenly distributed between 0 and 1. Figure 3 presents the resulted $\Delta_{\text{LCF}}$ as a function of the number of data points ($N$) on individual $gr(i)$-band light curves. Excluding the data points from M22 KT-43 (see Figure 2(a)), we bin the values of $\Delta_{\text{LCF}}$ into three bins of 10 < $N$ < 50, 50 < $N$ < 200, and $N$ > 200. The median values of $\Delta_{\text{LCF}}$ decrease from 0.045 mag to 0.009 mag from the first bin to the last bin, indicating the fitted Fourier expansion on individual $gr(i)$-band light curve will be closer to the template light curve when $N$ increases.

Mean magnitudes of the individual $gr(i)$-band light curves were equivalent to the sum of the $m_0$ term from the fitting of template light curves and the vertical shift $\Delta m$, they were listed in Table 4 as $\langle m \rangle$, where $m = \{g, r, i\}$. The minimum locus of the fitted template light curves were adopted as the magnitudes at maximum light of each CB, $m_X$, in Table 4. The dispersion $\sigma_m$ of fitting the template light curves to individual $gr(i)$-band light curves were also given in Table 4.

5. THE PERIOD-LUMINOSITY RELATIONs

Using the periods as well as the mean magnitudes and the magnitudes at maximum light obtained from previous sections, together with extinction corrections and published distances to individual globular clusters, the PL relations can be derived. Values of reddening $E$ toward each of the CB was obtained using the Bayerstar2019 3D reddening map (Green et al. 2019) with the adopted distances listed in Table 1.
map\(^3\) presented in Green et al. (2019), and listed in the last column of Table 4. Absolute magnitudes at mean or maximum light of the CB were then calculated via \(M_{(g,r,i)} = m_{(g,r,i)} - R_{(g,r,i)}E - 5\log D + 5\), where distance \(D\) is in parsec as given in Table 1. Since ZTF photometry is calibrated to the Pan-STARRS1 system (Masci et al. 2019), the values of extinction coefficient are \(R_{(g,r,i)} = \{3.518, 2.617, 1.971\}\) (Green et al. 2019). Errors from \(m\), \(E\) and \(D\) were propagated to the total errors on \(M\). In case of magnitudes at maximum light, the dispersion of the fitted light curves \(\sigma\), listed in Table 4, were adopted as the errors for \(m\). For those distances without errors, a 10\% error was assumed (Baumgardt et al. 2019).

5.1. Identifying Early-Type CB

Chen et al. (2016) and Chen et al. (2018) applied a period cut at \(\log P_{\text{cut}} = -0.25\) (or \(P_{\text{cut}} = 0.562\) days) to remove the early-type CB that have \(\log P > -0.25\) (also, see Rucinski 2006). In Table 4, there are three CB with periods longer than \(P_{\text{cut}}\) (V21 in M9, V41 in NGC6401 & V30 in NGC6712). However, Jayasinghe et al. (2020) proposed to use a period-temperature relation to separate out the early-type and late-type CB. Left panel of Figure 4 presents the effective temperatures, \(T_{\text{eff}}\), of the CB in our sample as a function of orbital periods, where the effective temperatures were converted from the extinction corrected \((g - r)\) colors, \(T_{\text{eff}}/10^4K = 1.09/[(g - r) + 1.47]\) (Fukugita et al. 2011), and the solid line is the period-temperature relation, \(T_{\text{eff}} = 6710K - 1760K\log(P/0.5\, \text{day})\), given in Jayasinghe et al. (2020). Five CB (V8 in M12, KT-23 in M22, V28 in NGC5466, V30 & V31 in NGC6712) clearly located above this relation, indicating they are early-type CB. On the color-magnitude diagram (CMD, see Figure 5), these early-type CB appeared to occupy the blue stragglers region. Nevertheless, investigation of the connection between CB and blue stragglers is out of the scope of this work. Theoretical and empirical of such investigations can be found in, for example, Stepien & Kiraga (2015) and Ferraro et al. (2009), respectively.

5.2. The r-Band PL Relation at Mean Light

\(^3\) http://argonaut.skymaps.info/
Figure 3. The averaged absolute difference between the template light curve and the individual gr(i)-band light curve, \( \Delta_{LCF} \), as a function of \( N \), the number of data points in the individual gr(i)-band light curves, where \( N \) is divided into three bins as indicated. Median values of \( \Delta_{LCF} \) in each bins are represented as solid horizontal lines. The dashed horizontal line represents \( \Delta_{LCF} = 0 \). The inset Figure is an enlarged version of \( \Delta_{LCF} \) vs. \( N \), after excluding the two outlier points for M22 KT-43.

Figure 4. Effective temperatures, \( T_{\text{eff}} \), of the CB in our sample as a function of orbital periods, where the effective temperatures were converted from the extinction corrected \( (g-r) \) colors using the converting relation given in Fukugita et al. (2011). The error bars represent the quadrature sum of the errors converted from the colors and \( \sigma_T \), where \( \sigma_T = 93\)K is the dispersion of the converting relation (Fukugita et al. 2011). The black solid line in the left panel is the period-temperature relation, proposed in Jayasinghe et al. (2020) to separate out the early-type and late-type CB. The blue and red solid lines in the right panel are the period-temperature relations for early-type and late-type CB, respectively, adopted from Jayasinghe et al. (2020), and the dashed lines represent the \( \pm 1\sigma \) dispersion of these relations.
Figure 5. Color-magnitude diagram for the CB in our sample. $M^0_r$ and $(g - r)_0$ denote the extinction corrected absolute magnitude and color, respectively. The red circles are the early-type CB identified in Figure 4 using the period-temperature relation. The model isochrones were taken from the Darmouth Stellar Evolution Database (Dotter et al. 2007, 2008). These isochrones were chosen to roughly bracket the metallicity listed in Table 1.

Figure 6(a) presents the $r$-band PL relation at mean light for the CB listed in Table 4 as a representative PL relation. Plots for the PL relation at $r$-band maximum light, as well as in the $g$- and $i$-band, were similar to Figure 6(a). The five identified early-type CB were marked as open circles in Figure 6(a), and their PL relation was presented separated in Figure 6(b). Since the effective wavelength of $r$-band is close to the Gaia’s $G$-band, the $G$-band PL relation adopted from Jayasinghe et al. (2020) was overlaid on Figure 6(b) as a guidance. Except the longest period early-type CB (V30 in NGC6712), other four early-type CB seems following the $G$-band PL relation for the early-type CB that is different from the late-type CB. Hence, these early-type CB were excluded in the subsequent analysis, as the number of them is too small to fit a meaningful PL relation.

The $r$-band PL relation at mean light for the remaining late-type CB, shown in Figure 6(c), exhibits a large scatter. The large scatter of the PL relation can also be seen from globular clusters that hosting 3 or more late-type CB (M4, M9, M22 & M71). Similar to Figure 6(b), the $G$- and $R$-band (again, due the effective wavelength of $R$-band is close to the $r$-band) PL relations taken from Jayasinghe et al. (2020) and Chen et al. (2018), respectively, were overlaid on Figure 6(c). Late-type CB with fainter absolute magnitudes at a given (orbital) period seems to follow the published $G$- or $R$-band PL relation. Since the absolute magnitudes were determined with only three parameters ($m$, $D$ and $E$), we examined each of them by using alternate values for one of them while keeping the remaining two parameters fixed, in order to determine if any of these parameters cause the observed large scatter of the PL relation. The results were presented in Figure 7.

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4 The effective wavelengths in $G$- and $r$- and $R$-band are 5857.56 Å, 6156.36 Å and 6695.58 Å, respectively. These values are adopted from the SVO Filter Profile Service (Rodrigo et al. 2012; Rodrigo & Solano 2020).

5 See footnote 4.

6 More precisely, using the same Bayerstar2019 3D reddening map, as $E$ in general is a function of distance $D$. 

Figure 6. Panel (a): The $r$-band PL relation for 30 CB in our sample. The red circles indicate the early-type CB selected based on the period-temperature relation (see Figure 4). Panel (b): Same as panel (a) but for the early-type CB, the solid line is the $G$-band PL relation taken from Jayasinghe et al. (2020). Panel (c): Same as panel (a) but for the late-type CB, the solid red and black lines are the $G$-band and $R$-band PL relation taken from Jayasinghe et al. (2020) and Chen et al. (2018), respectively. In both panel (b) and (c), the dashed lines are the corresponding $\pm 2\sigma$ dispersion of the adopted PL relations.
Changing the extinction: Upper-left panel of Figure 7 is similar to Figure 6(c), except the $E(B - V)$ values listed in Table 1 were used to correct for extinction.\footnote{The $E(B - V)$ values were converted to $E$ using the relation of $E(B - V) = 0.884E$ as given in http://argonaut.skymaps.info/usage.}

Changing the distance: Independent distance measurements were available from Wagner-Kaiser et al. (2017) for six globular clusters (M4, M12, M13, M15, M22 & M71). In case of M9, a weighted mean of $7.99 \pm 0.16$ kpc, measured from using the ab- and c-type RR Lyrae (Arellano Ferro et al. 2013), was adopted. For the bulge globular cluster NGC6401, the published distances covered a wide range including $\approx 6.35 \pm 0.81$ kpc (Tsapras et al. 2017, by using RR Lyrae) and $\approx 12.0 \pm 1.0$ kpc (Barbuy et al. 1999, by using horizontal branch on $VI$-band CMD). Therefore, these two NGC6410 distances were adopted to test their impact on the PL relation. The resulted PL relation was shown in upper-right panel of Figure 7. Note that V41 in NGC6401 was plotted twice using the two mentioned distances.

Changing the apparent magnitudes: The Clement’s Catalog or the references listed in Table 1 included the $V$-band magnitudes for the CB in our sample. However, these $V$-band magnitudes were mixed with magnitudes at mean light and at maximum light, and no associated errors were reported. The $V$-band PL relation, either at mean light or at maximum light, was displayed in lower panels of Figure 7, where the “error bars” in these plots represent the half amplitude of these CB. The $V$-band PL relation from Jayasinghe et al. (2020) was overlaid on the lower-left panel,

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure7}
\caption{Test of the PL relation by replacing extinctions (upper-left panel), distance (upper-right panel) and apparent magnitudes (lower panels) – see text for more details. The solid lines in the lower panels are the published $V$-band PL relations taken from Jayasinghe et al. (2020, in the lower-left panel) and Chen et al. (2018, in the lower-right panel); the dashed lines are the corresponding $\pm 2\sigma$ dispersion.}
\end{figure}
Figure 8. Locations of the 6 rejected CB (red triangles) while fitting the PL relations on the extinction corrected period-color relation (left panel) and the CMD (right panel), against other nominal CB (black circles).

Figure 9. Extinction corrected PL relations of the late-type CB located in globular clusters. The solid lines were fitted gri-band PL relations at maximum (left panels) and mean (right panels) light to the final 19 CB in the sample (filled black circles). These PL relations were fitted with a linear regression in the form of $M = a \log P + b$; the fitting results were given in the lower-right corners of each panels, where $\sigma$ is the dispersion of the fitted PL relations (the dashed lines represent the ±1σ of the PL relations). The filled red triangles were those CB being excluded in the fitting of the PL relations.

while the V-band PL relations from Chen et al. (2018) at both mean and maximum light were included in lower-right panel of Figure 7 as a guidance.
All of the PL relations displayed in Figure 7 were similar to Figure 6(c), which also displayed a large scatter, suggesting this could be intrinsic. There were 6 outliers CB in Figure 6(c) that are brighter than ~ 2σ boundaries of either the Chen et al. (2018) or Jayasinghe et al. (2020) PL relations, and seem to follow a different PL relation. The colors, and hence their temperatures, of these 6 CB do not appear to be anomalous when compared to other nominal CB, as shown in the left panel of Figure 8. On the CMD, these 6 CB are brighter than majority of the remaining CB located in the subgiant region (see Figure 5 and right panel of Figure 8), suggesting one of the component in these systems could be a subgiant. A detailed investigation of their nature is beyond the scope of this work. Nevertheless, after removing these 6 outliers CB a PL relation could be fit to the remaining 19 late-type CB.

5.3. The Derived gri-Band Period-Luminosity and Period-Wesenheit Relations

The gri-band PL relations at both mean and maximum light were fitted to the final sample of 19 CB, as shown in Figure 9. These gri-band PL relations at maximum light are:

\[ M_g = -8.89(\pm 1.43) \log P + 0.18(\pm 0.73), \sigma = 0.79, \]  
\[ M_r = -8.40(\pm 1.15) \log P - 0.08(\pm 0.59), \sigma = 0.63, \]  
\[ M_i = -7.32(\pm 1.44) \log P + 0.33(\pm 0.73), \sigma = 0.56, \]  

where \( \sigma \) is the dispersion of the fitted PL relation. The corresponding PL relations at mean light are:

\[ M_g = -8.95(\pm 1.47) \log P + 0.32(\pm 0.75), \sigma = 0.81, \]  
\[ M_r = -8.46(\pm 1.18) \log P + 0.06(\pm 0.61), \sigma = 0.65, \]  
\[ M_i = -7.35(\pm 1.47) \log P + 0.51(\pm 0.74), \sigma = 0.57. \]  

Due to small sample size and possible intrinsic large scatters, errors on the coefficients of the fitted PL relations, and the associated dispersions, were much larger than those presented in Chen et al. (2018) and Jayasinghe et al. (2020). The two longest period late-type CB could be eliminated based on period cut of log \( P = -0.25 \) (see Section 5.1), or based on their locations on the CMD (i.e. occupying the same subgiant regions as the 6 outlier CB, see Section 5.2). If they were removed from the sample, the slopes of the fitted PL relations would become shallower, at the same time doubling the errors on both of the fitted slopes and intercepts, even thought the dispersions of the PL relations remained nearly the same. Therefore, we decided to keep these two CB in our sample because they provide important constraints on the fitted PL relations.

Chen et al. (2018) showed that the slopes of the PL relations exhibit a trend as a function of wavelengths. Albeit their large errors, slopes of the fitted gri-band PL relations presented in Figure 9 were fully consistent with such trend as demonstrated in the left panel of Figure 10. Similarly, right panel of Figure 10 showed that the intercepts of the gri-band PL relations were in agreement with the multi-band PL relations from Chen et al. (2018). Interestingly, both slopes and intercepts of the PL relations derived in Jayasinghe et al. (2020) do not agree with those from Chen et al. (2018) at any given filters. We also noted the dispersions of the fitted gri-band PL relations, given in equation (2) to (7), decrease from the longer wavelength g-band filter to the shorter wavelength i-band filter, a similar trend is also seen in the PL dispersions reported in Chen et al. (2018) and Jayasinghe et al. (2020).

In addition to the gri-band PL relations, we have also fitted the period-Wesenheit (PW) relations for the late-type CB in our sample. The extinction-free Wesenheit indexes (Madore & Freedman 1991) were defined as:

\[ W^g_i = g - 2.274(g - i), \]  
\[ W^r_g = r - 2.905(g - r), \]  
\[ W^r_i = r - 4.051(r - i). \]

The resulted PW relations and their linear fittings were presented in Figure 11 and listed below:

\[ M_W^g_i = -6.40(\pm 1.35) \log P - 0.10(\pm 0.68), \sigma = 0.52, \]  
\[ M_W^r_g = -6.96(\pm 0.90) \log P - 0.83(\pm 0.46), \sigma = 0.50, \]  
\[ M_W^r_i = -7.04(\pm 1.54) \log P - 0.08(\pm 0.78), \sigma = 0.60, \]
Figure 10. Comparisons of the slopes (left panel) and intercepts (right panel) of the multi-band PL relations from Chen et al. (2018) and Jayasinghe et al. (2020) with the gri-band PL relations derived in this work (Figure 9). The intercepts of the PL relations from Jayasinghe et al. (2020) have been adjusted to the form of $M = A \log P + B$ (instead of $M = A \log P/0.5 + B$ in Jayasinghe et al. 2020).

Figure 11. Similar to Figure 9, but for the period-Wesenheit relations at maximum (left panels) and mean (right panels) light. The absolute magnitudes of Wesenheit indexes were calculated as $M_W = W^c - 5 \log D + 5$, where $c = gi$, $gr$ or $ri$. The filled black circles are the final 19 CB in the sample, and the filled red triangles were those CB being excluded in the fitting of the PW relations.
In the same manner, at mean light the PW relations are:

\[
M^W_{ri} = -7.06(\pm 1.51) \log P + 0.11(\pm 0.76), \quad \sigma = 0.58 \tag{16}
\]

In analogy to the $W_{JK}$ PW relation presented in Jayasinghe et al. (2020), dispersions of these PW relations were reduced to values between $\sim 0.5$ mag and $\sim 0.6$ mag when compared to the $gri$-band PL relations. For example, dispersion of the $W^gr$ PW relation was reduced by $\sim 38\%$ and $\sim 22\%$ when compared to the dispersions of the $g$- and $r$-band PL relations, respectively.

Even though about 100 CB in Chen et al. (2018) were located within the footprint of ZTF, these nearby sample of CB were too bright for ZTF as observations of ZTF saturate around $\sim 14$ mag. Instead, the $BV$-band photometry of the 183 CB in Chen et al. (2018) were transformed to $gr$-band using the quadratic transformation relation given in Tonry et al. (2012). We did not transform the Johnson $I$-band photometric data in Chen et al. (2018) to $i$-band because the transformation given in Tonry et al. (2012) was in Cousins system, and we tended to avoid “double transformations”. After transformed the $BV$-band photometry to $gr$-band, we checked the effective temperatures of these CB, following the same procedures done in Section 5.1. Five CB in the Chen et al. (2018) sample turned out to be early-type CB, and hence they were removed from the sample. Top and middle panels of Figure 12 compared the $gr$-band PL relations at maximum light (left panels) and at mean light (right panels) between our sample of CB in the globular clusters and the transformed $gr$-band photometry for the rest of the nearby CB sample, at which a good agreement is clearly seen. Combining these two independent sets of CB samples, referred as the combined CB sample, we derive the following PL relations at maximum light:
Figure 13. Residuals of the PL relations at maximum light (left panels) and at mean light (right panels) as a function of extinction corrected \((g - r)\) colors. The (red) horizontal lines represent zero residuals. In all panels, the 19 CB in the globular clusters and the 178 nearby CB were marked as black circles and purple crosses, respectively.

\[
M_g = -9.32(\pm 0.41) \log P + 0.15(\pm 0.19), \quad \sigma = 0.45, \quad (17)
\]

\[
M_r = -8.20(\pm 0.33) \log P + 0.14(\pm 0.15), \quad \sigma = 0.35. \quad (18)
\]

While the corresponding PL relations at mean light are:

\[
M_g = -9.45(\pm 0.43) \log P + 0.26(\pm 0.20), \quad \sigma = 0.47, \quad (19)
\]

\[
M_r = -8.34(\pm 0.34) \log P + 0.25(\pm 0.16), \quad \sigma = 0.37. \quad (20)
\]

Errors on the slopes and intercepts on these PL relations, derived from the combined CB sample, are much reduced when compared to their counterparts based on the 19 CB in globular clusters. The PL dispersions derived from the combined CB sample were also reduced by \(\sim 42\%\) to \(\sim 44\%\) in comparison to the PL dispersions using only the 19 CB in globular clusters.

In contrast, data points based on the Chen et al. (2018) sample exhibit a larger scatter on the PW relations when comparing to the PL relations (especially around \(\log P \sim -0.5\)), as demonstrated in the bottom panels of Figure 12. After applying an iterative 2.5\(\sigma\)-clipping algorithm, we derived the following PW relation at maximum light:

\[
M^{gr}_W = -5.16(\pm 0.33) \log P + 0.06(\pm 0.15), \quad \sigma = 0.32, \quad (21)
\]

Similarly, the PW relation at mean light is:

\[
M^{gr}_W = -5.26(\pm 0.34) \log P + 0.17(\pm 0.15), \quad \sigma = 0.33. \quad (22)
\]

These \(M^{gr}_W\) PW relations show a substantial improvement over the PW relations only based on the 19 CB in globular clusters as given in equation (12) and (15). The dispersions of 0.32 mag and 0.33 mag for these \(M^{gr}_W\) PW relations are also the smallest when compared to the \(gr\)-band PL relations derived from the combined CB sample, and comparable to the dispersions of the \(G\)- and \(R\)-band PL relations given in Chen et al. (2018) and the \(G\)-band PL relation from Jayasinghe et al. (2020).

6. THE PERIOD-LUMINOSITY-COLOR RELATIONS

Earlier works mentioned in the Introduction focused on the derivation of PLC relations. This is because from theoretical consideration the effective temperature of the CB system, and hence the color term, is expected to be present in the correlation between the orbital period and absolute magnitudes for the CB (for example, see Rucinski...
Figure 14. Color-corrected PL relations at maximum light (left panels) and at mean light (right panels). In all panels, the 19 CB in the globular clusters and the 178 nearby CB were marked as black circles and purple crosses, respectively.

1994; Rucinski & Duerbeck 1997b), although other works (Mateo & Rucinski 2017) indicated the color term might not need to be included. Indeed, residuals of the PL relations derived in Section 5.3 were well (anti-)correlated with the $(g-r)$ colors, as shown in Figure 13. The slopes were found to be $-1.47(\pm 0.14)$ mag and $-0.67(\pm 0.13)$ mag for the $g$- and $r$-band mean light PL relations, respectively. Similarly, slopes of the residuals for the $g$- and $r$-band maximum light PL relations are $-1.42(\pm 0.13)$ mag and $-0.63(\pm 0.12)$ mag, respectively. Including the $(g-r)$ color term in the linear regression, we obtained the following extinction corrected PLC relation at maximum light with the combined CB sample:

$$M_{(g,r)} = 0.13(\pm 0.14) - 7.32(\pm 0.34) \log P + \alpha_{(g,r)}(g - r),$$

where $\alpha_g = 1.78(\pm 0.14)$ and $\alpha_r = 0.78(\pm 0.14)$. Both of the derived PLC relation carries a same dispersion of 0.33 mag, which is similar to the PW relations. The corresponding PLC relation at mean light is:

$$M_{(g,r)} = 0.24(\pm 0.14) - 7.39(\pm 0.35) \log P + \alpha_{(g,r)}(g - r),$$

where $\alpha_g = 1.85(\pm 0.14)$ and $\alpha_r = 0.85(\pm 0.14)$, with the same dispersion of 0.34 mag. It is worth to point out that the PLC relations at maximum and mean light, presented in equation (23) and (24) respectively, are consistent to each others, and both slopes and color terms ($\alpha$) are the same within the errors. Furthermore, dispersions of these PLC relations are similar to the dispersions of the $M^r_W$ PW relations derived in Section 5.3. Figure 14 presents the PL relations after removing the color term, at which the reduction of the dispersion on the $g$-band PL relation can be clearly seen.

7. AN EXAMPLE OF APPLICATION

Recently, Vivas et al. (2020) conducted time-series observations in $gi$-band on a dwarf galaxy Crater II using the DECam installed on the 4m Blanco Telescope. These authors found 14 eclipsing binaries within the survey area. Based on their locations on the CMD, the authors concluded these eclipsing binaries are foreground objects. The $g$-band PL relation given in equation (19) can be used to confirm foreground nature of them. Visual inspecting the light curves of these eclipsing binaries revealed 6 of them (V118, V119, V120, V121, V124 & V126) have CB-like light curves. As illustrated in Figure 15, the reported periods in Vivas et al. (2020) need to be doubled for V119, V121, V124 & V126, because CB light curves are expected to exhibit two minima with nearly equal depth. Since the photometry of these DECam observations were calibrated to the SDSS (Sloan Digital Sky Survey) system (Vivas et al. 2020), we converted the mean $g$-band magnitudes for these six CB to the Pan-STARRS1 (PS1) system via the transformation equations provided in Abbott et al. (2021). We did not convert the corresponding mean $i$-band magnitudes because Vivas et al. (2020) observations did not include the $r$-band, hence no $(r-i)$ colors available to perform such transformation.
Assuming these eclipsing binaries are late-type CB, using the extinction provided by Vivas et al. (2020) and the $g$-band PL relation given in equation (19) we found that the distance moduli of these 6 CB ranged from 11.28 mag to 13.48 mag (with errors of $\sim 0.45$ mag, dominated by the dispersion of the $g$-band PL relation), which are much closer than the distance modulus of Crater II (20.33±0.07 mag, Vivas et al. 2020). Therefore, the foreground nature of these eclipsing binaries were confirmed.

8. CONCLUSION

In this work, we present, for the first time, the $gr(i)$-band PL, PW and PLC relations for the late-type CB. We started a sample of 79 CB in 15 globular clusters visible from the Palomar Observatory, however about three quarters of them were eliminated due to either extrinsic (CB with no or lack of ZTF data, and those affected by blending) or intrinsic (CB belongs to early-type, and the 6 outliers CB) reasons. The remaining 19 CB (in 8 globular clusters), at which the number is same or similar to some early work (Rucinski 1994; Rucinski & Duerbeck 1997a), were used to fit the $gri$-band PL relations and the PW relations. Even though the errors on the coefficients (slopes and intercepts) and the dispersions of the PL (and PW) relations for this sample of CB were several times larger than the published PL relations at similar filters, these slopes and intercepts of the $gri$-band PL relations were consistent to the local sample of CB as derived in Chen et al. (2018), suggesting CB in globular clusters is a viable and yet independent route to calibrate and/or cross-check the PL relations. By transforming the $BV$ photometry of the local CB samples in Chen et al. (2018) to $gr$-band, the PL and PW relations for these two independent CB samples were shown to...
be in good agreements, and hence both samples of CB can be combined to improve the derivation of the PL and PW relations in the $gr$-band, as the dispersions of these relations were greatly reduced when using the combined CB sample. We have also derived the PLC relations using the combined CB sample as the residuals of the PL relations were well (anti-)correlated to the $(g-r)$ colors. Finally, we applied the $g$-band PL relation to derive the distance moduli of 6 CB found in Vivas et al. (2020), proving that they were all foreground objects and unrelated to the dwarf galaxy Crater II. We envision these relations, especially the $gr$-band PW and PLC relations that exhibit the smallest dispersion, will be useful in future distance scale work to trace distances using the late-type CB, for example, located in the Galactic halo or dwarf galaxies. We expect a large number of late-type CB to be discovered in time-domain surveys that include the $gr(i)$ filters, such as the SkyMapper Southern Survey (Onken et al. 2019), the Dark Energy Survey (Dark Energy Survey Collaboration et al. 2016), and the Vera C. Rubin Observatory’s LSST (Ivezić et al. 2019), in the near future. The globular clusters based $gri$-band PL, PW and PLC relations could be potentially improved by increasing the number of (late-type) CB in globular clusters from future ZTF data releases, or dedicated observations with larger aperture telescopes.

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This research has made use of the SIMBAD database and the VizieR catalogue access tool, operated at CDS, Strasbourg, France. This research made use of Astropy, a community-developed core Python package for Astronomy (Astropy Collaboration et al. 2013, 2018).

This research has made use of the SVO Filter Profile Service (http://svo2.cab.inta-csic.es/theory/fps/) supported from the Spanish MINECO through grant AYA2017-84089

Facility: PO:1.2m

Software: astropy (Astropy Collaboration et al. 2013, 2018), gatspy (VanderPlas & Ivezić 2015), Matplotlib (Hunter 2007), NumPy (Harris et al. 2020), SciPy (Virtanen et al. 2020)

APPENDIX

ZTF LIGHT CURVES FOR THE 30 CONTACT BINARIES

In Figure 16, we present the folded ZTF light curves for all of the 30 CB listed in Table 4.

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Figure 16. ZTF light curves folded with published periods (top panels in each sub-figures) and periods found in this work (middle panels in each sub-figures). The solid curves in the middle panels of each sub-figures are the template light curves by fitting a 4th-order Fourier expansion to the combined light curves. These template light curves where then shifted vertically to fit the individual $gr(i)$-band light curves displayed in the bottom panels of each sub-figures. For comparison, the dashed curves in the bottom panels are the fitted 4th-order Fourier expansion to individual $gr(i)$-band light curves. The blue circles, green squares and red triangles represent the $g$, $r$- and $i$-band data, respectively. Crosses are the rejected outliers of the light curves.
Figure 16. Continue.
Figure 16. Continue.
