INSIDE-OUT PLANET FORMATION. III. PLANET–DISK INTERACTION AT THE DEAD ZONE INNER BOUNDARY

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ABSTRACT

The Kepler mission has discovered more than 4000 exoplanet candidates. Many of them are in systems with tightly packed inner planets. Inside-out planet formation (IOPF) has been proposed as a scenario to explain these systems. It involves sequential in situ planet formation at the local pressure maximum of a retreating dead zone inner boundary (DZIB). Pebbles accumulate at this pressure trap, which builds up a pebble ring and then a planet. The planet is expected to grow in mass until it opens a gap, which helps to both truncate pebble accretion and also induce DZIB retreat that sets the location of formation of the next planet. This simple scenario may be modified if the planet undergoes significant migration from its formation location. Thus, planet–disk interactions play a crucial role in the IOPF scenario. Here we present numerical simulations that first assess the degree of migration for planets of various masses that are forming at the DZIB of an active accretion disk, where the effective viscosity is undergoing a rapid increase in the radially inward direction. We find that torques exerted on the planet by the disk tend to trap the planet at a location very close to the initial pressure maximum where it formed. We then study gap opening by these planets to assess at what mass a significant gap is created. Finally, we present a simple model for DZIB retreat due to penetration of X-rays from the star to the disk midplane. Overall, these simulations help to quantify both the mass scale of first (“Vulcan”) planet formation and the orbital separation to the location of second planet formation.

Key words: planet–disk interaction – planets and satellites: formation – protoplanetary disks

1. INTRODUCTION

Since launch in 2009, Kepler has revealed more than 4000 exoplanet candidates (e.g., Mullally et al. 2015). A large percentage (＞30%) of these candidates are in systems with tightly packed inner planets (STIPs). These are systems that usually have three or more detected planets of radii ~1–10 R⊕, and with periods less than 100 days (Fang & Margot 2012). There are two main scenarios that can produce such close-in planets: (1) formation in the outer disk followed by inward migration (e.g., Kley & Nelson 2012; Cossou et al. 2013, 2014), and (2) formation in situ (Hansen & Murray 2012, 2013; Chiang & Laughlin 2013; Chatterjee & Tan 2014, hereafter CT14).

The inward migration scenario tends to produce planets that are trapped in orbits of low-order mean motion resonances, which is not a particular feature of STIPS (Baruteau et al. 2014; Fabrycky et al. 2014). Thus, it has been proposed that the lack of resonant pileups might be explained by a lower efficiency of resonance trapping or breaking of resonance by later dynamical processes for the typically low-mass Kepler-detected planets (Goldreich & Schlichting 2014; Chatterjee & Ford 2015).

The in situ formation scenario faces the challenge of concentrating enough solids in the inner region (Raymond & Cossou 2014; Schlichting 2014). For example, supply of pebbles by radial drift may be truncated if planet formation, perhaps initiated by the pebble streaming instability (Youdin & Goodman 2005), occurs in the outer disk (Lambrechts & Johansen 2014; Bitsch et al. 2015; Levison et al. 2015). In situ formation models also face the challenge of reproducing the observed mass versus orbital radius distributions once effects of gas on protoplanet migration during the oligarchic growth phase are accounted for (Ogihara et al. 2015).

The inside-out planet formation (IOPF) scenario proposed by CT14 is a new type of in situ formation model. It starts with pebble delivery to the midplane transition region between the innermost MRI-active zone and a nonactive “dead zone,” where there is a local pressure maximum. The pebbles trapped by the pressure maximum will build up in a ring, which then forms a protoplanet, perhaps involving a variety of processes, including streaming (Youdin & Goodman 2005), gravitational (Toomre 1964), and/or Rossby wave (Varnière and Tagger 2006) instabilities. The protoplanet is expected to continue its growth, especially by pebble accretion, until it becomes massive enough to open a gap in the disk. This gap pushes the pressure maximum outward by a few Hill radii, thus creating a new pebble trap that is displaced from the planet’s orbit (Lambrechts et al. 2014), but may also allow MRI activation in the region beyond the planet, which could induce further outward retreat of the dead zone inner boundary (DZIB).

As discussed by CT14, planetary migration, either before gap opening (Type I) or after gap opening (Type II), may in principle alter this scenario. However, the expectation is that the pressure maximum associated with this inner disk transition region will also act as a planet trap (Masset et al. 2006; Matsumura et al. 2009; Kretke & Lin 2012; Bitsch et al. 2014), so the planet will stay at its initial formation location and keep accreting more materials, at least until the point of gap opening. However, this needs to be confirmed for the particular disk structure involved in IOPF, and this is one of the goals of this paper.

The disk studied by Masset et al. (2006) was a purely passive disk, i.e., the temperature was set only by irradiation from the central star. Zhang et al. (2014) studied planetary migration in a
disk with an inner region heated by viscous dissipation and an outer region heated by stellar luminosity. This structure also contained a local pressure maximum that acted as a trap for outer region heated by stellar luminosity. This structure also disk with an inner region heated by viscous accretion, with accretion rates $\sim 10^{-9} M_\odot \text{yr}^{-1}$.

The magnitude of the planet mass that leads to gap opening and potential DZIB retreat is also of crucial importance for the IOPF theory. Gap opening has been studied by Lin & Papaloizou (1986, 1993), who proposed a “viscous-thermal” criterion that sets a gap opening mass. This mass is sensitive to the local disk viscosity. Magnetohydrodynamic simulations with realistic turbulence have also been carried out to study gap opening in turbulent disks (Nelson & Papaloizou 2003; Zhu et al. 2013).

The second goal of this paper is to study gap opening and quantify the gap opening mass in the context of the IOPF disk model, i.e., an inner region of an active disk where the effective viscosity is undergoing a sharp increase in the radially inward direction. These gap opening masses can then be compared to masses of the innermost, so-called Vulcan planets. An initial comparison of the simple, analytic gap opening mass prediction with the observed Vulcans has been carried out by Chatterjee & Tan (2015, hereafter CT15, Paper II), who found a predicted scaling and normalization of planet mass versus orbital radius, $r$, of $M_p = M_G \approx 5.0 \phi_{G,0.3}(\tau/0.1 \text{AU})_{0.3} M_\oplus$, where $\phi_{G,0.3}$ is a dimensionless parameter that indicates the fraction of the Lin–Papaloizou mass scale that is assumed to lead to a deep enough gap to truncate planetary accretion of pebbles and initiate DZIB retreat. The normalization of this gap opening planet mass at a given radius also depends on the Shakura–Sunyaev viscosity parameter, $\alpha$, in the DZIB region, with the fiducial value of $10^{-3}$ being adopted in the above formula. However, this value is quite uncertain, and the observed planet masses may require a somewhat lower value of $2 \times 10^{-4}$ (Paper II), or a lower value of $\phi_G$.

Finally, our third goal is investigate how gap opening may induce DZIB retreat, which then sets the location of second planet formation. Here we will present a simple, heuristic first exploration of this process by modeling the location of the DZIB as set by penetration of X-rays emitted from the protostellar corona to the disk midplane beyond the planet-induced gap. This location then sets the radius for an imposed radial profile of viscosity that simulates the transition region from an MRI-active inner region to an outer dead zone. Increased viscosity leads to reduced densities that make it easier for X-rays to penetrate further. We present example toy models of this process in which the location of the DZIB ends up stabilizing several initial gap widths away from the planet. Such separations can be compared to the observed separation of orbits of innermost planets in STIPs.

In Section 2, we describe an analytic model to calculate our disk parameters. In Section 3, we describe our numerical setup and test the numerical simulations against the analytic model. In Section 4, we study migration of planets of various masses located in the DZIB region. In Section 5, we study gap opening and DZIB retreat. In Section 6, we discuss the implications of our results for observed planets. We conclude in Section 7.

2. ANALYTIC ESTIMATES OF DISK STRUCTURE AND GAP OPENING MASS

As in Paper I, we follow the Frank et al. (2002) derivation of the structure of a viscously heated accretion disk. These results will be compared with the numerical simulations from FARGO, described in Section 3. To achieve consistency with these simulations, we find that we need to make a small correction in the choice of the vertical optical depth equation and now adopt

$$\tau = 0.5 \Sigma \kappa,$$

(1)

with the factor of 0.5 being introduced since the disk has two faces (or equivalently a change in the definition of “midplane” conditions). Thus, when calculating the balance between energy dissipation and radiative cooling, the optical depth is integrated from the midplane to each surface of the disk. This change then leads to modest ($\leq 40\%$) changes in the normalization of the disk structure equations compared to CT14. For example, for disk mass surface density we now derive

$$\Sigma_G = \frac{2^{7/5}}{3^{4/5} \pi^{3/5}} \left( \frac{\mu}{\gamma k_B T} \right)^{4/5} \left( \frac{\kappa}{\sigma_{SB}} \right)^{-1/5} \alpha^{-4/5} \times \left( \frac{GM_*}{r} \right)^{3/5} \left( \frac{f m_s}{m_\odot} \right)^{3/5} \left( \frac{r}{\text{AU}} \right)^{-3/5} \mathrm{g cm}^{-2}$$

(2)

(CT14 derived a normalization of $106 \text{ g cm}^{-2}$), where $\mu = 2.33 m_H = 3.90 \times 10^{-24} \text{ g}$ is the mean particle mass (assuming $n_{H_2} = 0.1 n_H$), $k_B$ is Boltzmann’s constant, $\gamma = 1.4 \gamma_{1.4}$ is the power-law exponent of the barotropic equation of state $P = K \rho^\gamma$, $\sigma_{SB}$ is the Stefan–Boltzmann’s constant, $m_\odot \equiv m_{\odot,1} M_\odot$ is the stellar mass, $\Sigma_G$, $\Sigma_{SB}$ is disk opacity (normalized to expected protoplanetary disk values; e.g., Wood et al. 2002), $f_r \equiv 1 - \sqrt{r_s/r}$, (where $r_s$ is stellar radius), and $m \equiv m_{\odot,9} 10^{-9} M_\odot \text{ yr}^{-1}$ is the accretion rate.

For the disk aspect ratio we find

$$\frac{h}{r} = \left( \frac{3}{128} \right)^{1/10} \pi^{-1/5} \left( \frac{\mu}{k} \right)^{-2/5} \gamma^{-1/10} \sigma^{-1/10} \frac{GM_*}{r} \times \alpha^{-1/10} \left( \frac{GM_*}{r} \right)^{-7/20} \kappa^{1/10} \left( \frac{f m_s}{m_\odot} \right)^{1/5} \gamma^{1/20}$$

$$\rightarrow 0.027 \gamma_{1.4}^{1/10} \kappa^{1/10} \alpha^{-3/10} \left( m_{\odot,1} \right)^{-7/20} \left( \frac{f m_s}{m_\odot} \right)^{1/5} \gamma^{1/20} \frac{GM_*}{r} \frac{h}{r}.$$  

(3)

The above equations will be used to set the initial conditions of the FARGO simulations described below.

Given this disk structure, the viscous criterion for the gap opening planet mass is

$$M_G = \phi_G \frac{40 m_m}{r^2 \sigma_{SB}}.$$  

(4)
Implementing our disk model, we obtain
\[
M_G = 40 \phi_G \left( \frac{3}{128} \pi^{-2/5} \left( \frac{\mu}{k} \right)^{-4/5} \gamma^{4/5} \sigma^{-1/5} \right)
\times \alpha^{2/5} G^{-7/10} m_{\alpha}^{3/10} \sigma^{1/5} (f_{\alpha} m_{\alpha})^{2/5} \epsilon^{1/10}
\rightarrow 14.08 \phi_G \gamma^{2/5} \epsilon^{1/10} \alpha^{-2/5} m_{\alpha}^{3/10} (f_{\alpha} m_{\alpha})^{2/5} r_{\text{AU}}^{1/10} M_\odot. \tag{5}
\]
This is a factor of 0.745 smaller than the CT14 result.

3. NUMERICAL SIMULATION METHODOLOGY

We used the 2D code FARGO-ADSG (Baruteau & Masset 2008a, 2008b), which is built on FARGO (Masset 2000), but with the energy equation and disk self-gravity implemented. Self-gravity has not been turned on in our calculation since the disk is far from gravitational instability in our problem, which focuses on inner regions near the star. We also implemented a simple method of radiative cooling that uses the disk surface density to calculate the optical depth and cooling rate as described in Zhu et al. (2012). We set up a disk with the same mass surface density profile, flaring index, opacity, adiabatic index, mean molecular mass, and central stellar mass as the fiducial analytic model in Section 2.

The energy equation implemented in FARGO-ADSG is (Baruteau & Masset 2008a)
\[
\frac{\partial e}{\partial t} + \nabla \cdot (e \nabla) = -(\gamma - 1) e \nabla \cdot \nabla + Q_+ - Q_-, \tag{6}
\]
where \(e\) is the thermal energy per unit area, \(\nabla\) is the flow velocity, and \(Q_+\) (\(Q_-\)) denotes heating (cooling) source terms, assumed to be positive quantities. In a steady accretion disk, these terms can be written as
\[
e = \frac{\Sigma_g T}{\gamma - 1} \frac{k_B}{\mu} = G m_* \frac{1}{\gamma - 1} \Sigma_g \left( \frac{m_*}{r} \right)^{1.7} r^{-1}, \tag{7}
\]
\[
Q_+ = \sum_{i,j} \frac{\partial \Sigma_g}{\partial r} = \nu \Sigma_g \left( \frac{d\Sigma_g}{dr} \right)^2, \tag{8}
\]
\[
Q_- = \frac{16 \sigma_{\text{SB}} T^4}{3 \pi}, \tag{9}
\]
where \(\Sigma_g\) are components of the viscous stress tensor and \(T\) is the midplane temperature. Note that \(\tau = 0.5 \Sigma_g T\) is the optical depth from disk midplane to the surface.\(^5\)

First, we set up an accretion disk with a constant value of \(\alpha\), i.e., without a transition zone, and a steady accretion rate of \(10^{-9} M_\odot\) yr\(^{-1}\), simulating a range of radii from 0.02 to 0.3 AU. In all simulations we use the EVANESCENT boundary condition. This damps the disk values (surface density, velocities, and energy density) to the initial axisymmetric disk conditions. The damping regions are wings within the radial ranges \([r_{\text{min}}, 1.25r_{\text{min}}]\) and \([0.84r_{\text{max}}, r_{\text{max}}]\), where \(r_{\text{min}}(r_{\text{max}})\) is the inner (outer) radius of the disk. The damping parameter is increased from zero to a maximum from the edge of the damping zone to the edge of the disk.

Within each orbit, the damping amplitude is not a constant: the actual damping is the calculated damping function times a
\(^5\) During numerical testing, we found an error in the public version of the code: it only calculates half the value of \(\nu \Sigma_g (dr_0/dr)^2\).

Figure 1. Mass surface density profile after 1000 orbits of our fiducial “transition” disk, where \(\alpha\) rises from 0.001 at 0.1 AU to 0.01 at 0.07 AU with a steady accretion rate of \(10^{-9} M_\odot\) yr\(^{-1}\). The dashed line is the profile of a “constant \(\alpha\)” disk (i.e., \(\alpha = 0.001\)).

4. PROTOPLANET MIGRATION

We study the migration of protoplanets of various fixed masses (0.1\(M_\odot\), 0.5\(M_\odot\), and 1.0\(M_\odot\)) that are inserted into the transition zone region of the disk by measuring the torques exerted on the planet by the disk. For each planet mass, we run simulations holding the planet at a constant radius, exploring uniformly from 0.085 to 0.115 AU with a spacing of 0.001 AU. So for each planet mass there are 31 MR and HR simulations run, for a total of 186 simulations. Note that we keep the \(\alpha\) viscosity radial profile constant in all the simulations in this section. We run each simulation for 400 orbits, thus allowing the gas disk to achieve a quasi equilibrium structure. We then evaluate the torque on the planet by averaging over the next 100 orbits. Given the 2D nature of these simulations, we adopt a smoothing length in the calculation of the planet’s gravitational potential of 0.6h (Müller et al. 2012).

The torque, \(\Gamma\), is scaled as \(\Gamma_0 = (M_p/m_*)^2 \Sigma_g r^2 \Omega_g^2 h^{-2}\), where \(r\) is the orbital radius of the planet and \(\Sigma_g\) is the average
Our standard MR run is more than twice the Hill radius of a gas mass surface density at this orbital radius. The grid size in our standard MR run is more than twice the Hill radius of a planet with $M_p = 0.1 M_G$. We therefore carry out HR simulations with twice greater resolution and examine numerical convergence.

In all cases for $0.1 M_G$, $0.5 M_G$, and $1.0 M_G$-mass planets (which correspond to very different levels of gap opening—see below), the torque profiles show a common behavior of $\Gamma$ decreasing from positive to negative values in the transition region (where $\alpha$ starts decreasing as $r$ increases just interior of 0.1 AU), indicative of a stable “planet trap” in this location, where $\Gamma = 0$ (see Figure 2). We note that the magnitude of $\Gamma$ decreases significantly as $M_p$ increases from the Type I to Type II regimes.

This confirmation of planet trapping at the DZIB transition zone is a key requirement of IOPF, since this allows a planet to continue to grow by pebble accretion from low to relatively high masses. Next, we investigate how pebble accretion may be disrupted by gap opening by looking at the detailed structure of the gaps.

5. GAP OPENING

5.1. Gap Structure and Opening Mass for Fixed $\alpha$ Profile

The gap opening process in IOPF is critical to termination of pebble accretion of the first planet, thus setting its mass. It may also be important, in combination with dead zone retreat, in setting the location of the pressure maximum that leads to new pebble ring formation and then second planet formation.

We now investigate the disk structure that is induced by introducing planets of various masses at a fixed location of $r = 0.1$ AU, i.e., at the transition zone of the disk with a fixed $\alpha$ profile. Figure 3 shows the radial profiles of mass surface density, midplane pressure, and midplane temperature after 1000 orbits of evolution from introduction of planets of masses $M_p = 0.1 M_G$ to $1.0 M_G$ in steps of $0.1 M_G$. We note that the gas profile settles very quickly, within $\sim$100 orbits, to a profile close to that of the final state at 1000 orbits.

As planet mass increases, the radial profiles show a gradual deepening of the gap in both the mass surface density and pressure profiles. The temperature also dips owing to reduced viscous heating and smaller optical depths. For this particular setup, with a transition zone width of 0.03 AU, it is only once planet masses are $\gtrsim 0.5 M_G$ that there is significant displacement of the azimuthally averaged pressure maximum away from the planet’s orbital radius. Table 1 lists the separation of the pressure maximum from the planet’s orbital radius at 0.1 AU, $\Delta P_{\text{max}}$, but normalized by the planet’s Hill radius, $R_H = (M_p/(3 m_*)^{1/3})$. We define $\phi_{\Delta r, P_{\text{max}}} = \Delta P_{\text{max}}/R_H$. As $M_p$ increases from $0.4 M_G$ to $0.5 M_G$, $\phi_{\Delta r, P_{\text{max}}}$ grows by a factor of 10 from $\approx 0.4$ to $\approx 5$. Figure 3 shows that this also
corresponds to the mass surface density maximum retreating outward by a similar amount.

We have compared gap opening results for simulations with \( M_p = 0.1, 0.5, 1.0 M_\odot \) at MR and HR resolutions. We find very similar radial profiles of \( \Sigma \) and \( P \), with agreement in values at better than 10% across the width of the gap region.

Figure 4 shows the 2D view of the perturbation of the disk mass surface density (compared to the disk with no planet) in the \( r-\phi \) plane. The strengthening spiral arms, along with deepening gap, are evident.

5.2. DZIB Retreat with an Evolving \( \alpha \) Profile

When a planet opens a gap in the disk leading to decreasing density in the vicinity of the planet, we expect higher ionization levels given the \( r^2 \) dependence of recombination rates, and thus greater likelihood of activating the MRI, which then results in the retreat of the DZIB. Higher levels of ionization may also arise owing to shock heating in spiral arms that are induced by the planet. We note that these spiral arms, propagating outward into the dead zone, will by themselves also provide a source of enhanced effective viscosity. The lower densities of the gap region may also allow for increased penetration of X-rays that raise the ionization level and activate the MRI. Such effects could cause the viscosity to make its radial transition further out in the disk, which would lower the density in the gap region and vicinity even more.

The full treatment of these processes is a very complex problem, beyond the scope of the present paper. Here we present a simple, heuristic model for DZIB retreat based on X-ray penetration from the protostellar corona to the disk midplane. The X-rays are assumed to propagate from a height of 0.05 AU at \( r = 0 \) (i.e., \( 11 R_\odot \), which is expected to be \( \sim 3-4 \) stellar radii for a solar-mass pre-main-sequence star). The thickness of the transition zone from the MRI-active region to the dead zone is assumed to be characterized by \( \phi_X \Sigma_X \), i.e., a mass surface density that scales with the X-ray penetration mass surface density due to absorption, \( \Sigma_X \).

Figure 4 shows the 2D view of the perturbation of the disk mass surface density (compared to the disk with no planet) in the \( r-\phi \) plane. The strengthening spiral arms, along with deepening gap, are evident.

Table 1

| \( M_p/M_\odot \) | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 | 1.0 |
|-----------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| \( \phi_{\Delta r_{\text{max}}}^\alpha = \Delta r_{\text{max}}/R_H \) | 0.61 | 0.48 | 0.42 | 0.38 | 4.75 | 4.47 | 5.09 | 4.86 | 4.68 | 5.27 |

Note.

\( ^\alpha \) The separation between new pressure maximum and planet orbital radius, scaled to planet’s Hill radius. These results are for disks with fixed \( \alpha \) profile with a transition width of \( \Delta r_{\text{DZIB}} = 0.03 \) AU. Note that the location of pressure maximum is measured at the center of the grid cell of maximum pressure.

\( \phi_X \Sigma_X \) X-ray penetration from the protostellar corona to the disk midplane. The X-rays are assumed to propagate from a height of 0.05 AU at \( r = 0 \) (i.e., \( 11 R_\odot \), which is expected to be \( \sim 3-4 \) stellar radii for a solar-mass pre-main-sequence star). The thickness of the transition zone from the MRI-active region to the dead zone is assumed to be characterized by \( \phi_X \Sigma_X \), i.e., a mass surface density that scales with the X-ray penetration mass surface density due to absorption, \( \Sigma_X \).

Starting from the FARGO simulation with \( \phi_G = 0.5 \) after 300 orbits (i.e., when a wide, but relatively shallow, gap has just been opened), the radius of the DZIB, \( r_{\text{DZIB}} \), is reevaluated each orbit by the condition that the mass surface density along the path from the X-ray corona to the midplane equals \( \phi_X \Sigma_X \).

For simplicity, we assume that there is negligible material along this path length at locations interior to the planet, i.e., at \( r < 0.1 \) AU, which we consider to be a good approximation both because of the viscous clearing of the inner disk and since the disk’s vertical scale height is small in this region. Thus, our path integral starts from \( r = 0.1 \) AU and extends out to \( r_{\text{DZIB}} \). Note that this path starts with a relatively shallow angle to the midplane of \( \simeq 24^\circ \), which then decreases as the disk evolves and \( r_{\text{DZIB}} \) increases.

In addition, we need to specify the structure of the \( \alpha \) transition zone in the X-ray penetration region. We expect it to be broader than the transition zone set by thermal ionization of alkali metals. For simplicity, we assume that the functional shape of the radial variation of \( \alpha \) is the same as that adopted in Section 3. The outer radius where \( \alpha \) starts rising from the DZIB value of 0.001 is set by the mass surface density along the path length being equal to \( \phi_X \Sigma_X \). We note that the width of this...
transition region may be somewhat larger than the actual penetration depth of the X-rays (i.e., $\phi_X > 1$), because of, for example, the outward propagation of turbulence, which has been seen in the simulations of Dzyurkevich et al. (2010). For the inner radius, $r_i$, where $\alpha$ reaches the full MRI value of 0.01, we investigate three cases, i.e., inner radii of 0.07 AU (Case A: the same as adopted for our migration and gap opening studies, above), 0.1 AU (Case B: the location of the planet), and 0.11 AU (Case C: the location of the initial gap outer edge that has been induced by the planet).

For a simple estimate on the values of $\Sigma_X$ and $\phi_X$ to be used in this model, we note that X-ray opacity, even at $\sim 10$ keV, may be dominated by heavy elements in the gas, rather than in dust, especially if dust has mostly coagulated into large grains and pebbles that have settled to the midplane and been trapped at the DZIB pressure maximum. For interstellar gas with solar abundances and the case of heavy-element depletion, Igea & Glassgold (1999) find an absorption opacity of

$$\tau_E = 0.056 (\Sigma/1 \text{ g cm}^{-2}) (E/10 \text{ keV})^{-2.81}$$

(valid for $E = 2 - 30$ keV). Thus, $\tau_{30 \text{ keV}} = 1$, 10 requires $\Sigma_X = 18$, 180 g cm$^{-2}$ and $\Sigma_{X, 39} = 39$, 390 g cm$^{-2}$. Thus, we choose a characteristic value of $\Sigma_X = 100$ g cm$^{-2}$, equivalent to absorption optical depths of a few for $\sim 20$ keV X-rays. We note, however, that the radiative transfer of these higher-energy X-rays is likely to be controlled by Compton scattering by electrons present in neutral H, H$_2$, and He, which may allow increased penetration to the disk midplane at greater radial distances via scattering from the disk atmosphere. For this reason, along with the extra thickness of the transition zone that is expected owing to propagation of turbulent wakes from the MRI-active zone (including vertically from modest scale heights), we choose a fiducial value of $\phi_X = 5$.

From the above discussion, it is clear that more detailed calculations are needed to better constrain the combined parameter $\phi_X \Sigma_X$, including ionization equilibrium calculations, e.g., similar to those of Igea & Glassgold (1999), and then applying the resulting resistivities to determine the extent of the MRI-active zone (S. Mohanty & J. C. Tan 2015, in preparation). The time-variable nature of the X-ray luminosity may also need to be accounted for.

Figure 5 shows results from these DZIB retreat models. We find that $n_{\text{DZIB}}$ increases gradually over timescales of several thousand orbits of the planet. For Case A, by 6500 orbits the rate of increase is very slow, i.e., from the 6500th to 7000th orbit the percentage increase is $< 0.06\%$ for the MR run and 0.07\% for the HR run. The equivalent results for Cases B and C are similar. However, the value of $n_{\text{DZIB}}$ after 7000 orbits does depend somewhat on the resolution of the simulation: for the Case A MR run $n_{\text{DZIB}} = 0.128 \text{ AU}$; for the HR run $n_{\text{DZIB}} = 0.139 \text{ AU}$, i.e., the amount of retreat ($\Delta r_{\text{p,max}}$) is about 38.6\% greater in the HR run. We thus also carried out twice higher, SHR runs for $\sim 1000$ orbits. We find that $\Delta r_{\text{p,max}}$ is $\leq 5\%$ greater than in the HR simulation. We use these results to estimate that the final numerically converged retreat distance is $\sim 5\% - 10\%$ greater than the HR result (or about 40\% greater than the MR result), i.e., $n_{\text{DZIB}}$ (Case A) $\approx 0.145 \text{ AU}$, i.e., $\Delta r_{\text{p,max}} \approx 0.045 \text{ AU}$. For this case with $M_p = 0.5 M_J = 5.59 M_J$, for which the planet’s Hill radius is $R_H = 1.78 \times 10^{-3} \text{ AU}$, then $\phi_{\Delta r_{\text{p,max}}} = \Delta r_{\text{p,max}}/R_H = 25.3$, which is a significantly greater retreat (i.e., $\sim 5 \times$ greater) than that due to simple gap opening in the fixed $\alpha$ model.

For Cases B and C the amount of retreat is larger and takes somewhat longer to stabilize (although the retreat has essentially stopped by 7000 orbits). After 7000 orbits, the HR simulations find a 24.0\% and 20.8\% larger retreat than the MR runs for Cases B and C, respectively. The SHR results at $\sim 1000$ orbits are 5.6\% and 4.9\% greater, respectively. Thus, we estimate that final converged values are about 25\% greater than the MR results, i.e., for Case B DZIB retreat to 0.20 AU ($\Delta r_{\text{p,max}} \approx 0.10 \text{ AU}$; $\phi_{\Delta r_{\text{p,max}}} = 56.3$) and for Case C DZIB retreat to 0.22 AU ($\Delta r_{\text{p,max}} \approx 0.12 \text{ AU}$; $\phi_{\Delta r_{\text{p,max}}} = 67.6$). These results are also summarized in Table 2.

As a check on self-consistency, we have also investigated the potential effect of X-ray penetration inducing an evolving $\alpha$ profile in a disk that does not yet have a planet or gap. For this model, where the accretion disk extends uninterrupted to very close to the protostar at $\sim 0.02$ AU, we set the height of the stellar X-ray corona to be equal to this inner disk radius, i.e., 0.02 AU. We also start the path integral for X-ray penetration from this distance. We find that for the same choices of $\Sigma_X$ and $\phi_X$ adopted above, the X-rays do not penetrate beyond $\sim 0.1$ AU, and so the DZIB $\alpha$ profile set by thermal ionization of alkali metals is not expected to be affected. However, we find that utilizing a larger X-ray corona height of 0.05 AU does enable X-ray penetration to beyond 0.1 AU in the no-planet disk. Thus, in the context of this simple model, DZIB retreat is also influenced by properties of the scale height of X-ray emission from the protostar.

Overall, we therefore see that the amount of DZIB retreat, which in the IOPF scenario is expected to set the location of second planet formation, depends somewhat sensitively on the detailed structure of the $\alpha$ transition zone and the X-ray emission properties of the protostar. Thus, future work to model this zone, including the full physics of activation of the MRI in response to a changing ionization fraction, e.g., due to X-rays or other ionization sources, is needed. However, we can still conclude that, for the parameters explored here, the amount of retreat is significantly greater than the retreat due to initial gap opening. In Section 6 we compare these retreat distances with the orbital spacings of the Kepler-observed planets.
The extent of the planet’s Hill sphere is shown by the vertical shaded band. Second row: the evolving \(\alpha\) disk model (HR run) at 7000 orbits due to X-ray penetration in which the inner \(\alpha\) transition radius is held fixed at 0.07 AU (Case A). Third row: same as above, but for Case B with inner transition radius at 0.1 AU. Bottom row: same as above, but for Case C with inner transition radius at 0.11 AU.

Figure 6 shows the radial structure of the disks for these evolving \(\alpha\) models after 7000 orbits and compares with the fixed \(\alpha\) profile model, which was already settled after 1000 orbits. This figure shows that the local pressure maximum remains closely located with the outer \(\alpha\) transition radius, i.e., where it begins to rise from its DZIB value of 0.001.

Table 2

| Models | Medium Res. (7000 orbits) | High Res. (7000 orbits) | Estimated Convergence |
|--------|---------------------------|-------------------------|-----------------------|
| Case A (0.5M\(_\odot\), \(r_i = 0.07\) AU) | 15.9 (0.028 AU) | 22.1 (0.039 AU) | \(\approx 25.3\) (0.045 AU) |
| Case B (0.5M\(_\odot\), \(r_i = 0.10\) AU) | 41.2 (0.073 AU) | 51.1 (0.091 AU) | \(\approx 56.3\) (0.100 AU) |
| Case C (0.5M\(_\odot\), \(r_i = 0.11\) AU) | 52.4 (0.093 AU) | 63.3 (0.112 AU) | \(\approx 67.6\) (0.120 AU) |

Note. \(\Delta D_{\text{Pmax}}\) measures the separation between the planet (at 0.1 AU) and the outer transition of the \(\alpha\) profile (as set by X-ray penetration) in units of the planet’s Hill radius. The outer transition radius is at a location very similar to that of the local pressure maximum (see Figure 6).

6. IMPLICATIONS FOR OBSERVED PLANETS

CT14 examined the separation of planet orbits in STIPs (normalized by Hill radius of inner planet in the pair), finding a broad range of separations from the innermost (Vulcan) planet...
to the next planet of \( r_1 \sim \text{few} \sim 100 \), with a broad peak from \( \sim 20 \) to \( 60 \). Note, however, that this analysis was based on the simple, single power-law planetary mass–size relation of Lissauer et al. (2011).

CT15 analyzed the available mass–size data for planets in STIPs and derived an improved, piecewise power-law mass–size relation. Here we use this relation (PL3 in CT15) to reevaluate the distributions of \( r_1 \) through \( r_4 \), where the numerical value of the subscript refers to the number of the planet that is the innermost in the pair being considered, counting out from the star. These results are presented in Figure 10.

Note that some of the dispersion in separations is likely to be induced by an intrinsic dispersion in the densities of the planets, leading to inaccurate estimation of masses. For example, the observed dispersion in density of a factor of about 5 (e.g., CT15) leads to a dispersion in inferred mass of the same factor and a dispersion in \( R_H \) and \( \phi_{\Delta r} \) of a factor of 1.7. Also, the observed values of \( \phi_{\Delta r,1} \) may be overestimated if some fraction of second planets are nontransiting and thus not detected owing to slight orbital misalignments.

In Figure 10 we also show the locations of \( \phi_{\Delta r,\text{max}} \) for the fixed and evolving \( \alpha \) disk models we considered. We note that the evolving \( \alpha \) disk models can achieve separations of \( \sim 20R_H \)–70\( R_H \), which overlap with the observed distribution of \( r_1 \).

As discussed by CT14, the distributions of \( r_1 \) are significantly different from those of the outer separations. This conclusion remains unchanged by our use of the improved piecewise power-law CT15 mass–size relation. For KPC systems with \( N_p \geq 3 \), the probability that \( r_1 \) and \( r_2 \) are drawn from the same distribution is \( 9 \times 10^{-4} \). Similarly, for systems with \( N_p \geq 4 \), the respective probabilities that two \( r_i \) distributions are drawn from the same underlying distribution are \( 7 \times 10^{-5} \), \( 3 \times 10^{-6} \), and 0.36 for \( r_1 \) and \( r_2 \), \( r_1 \) and \( r_3 \), and \( r_2 \) and \( r_3 \), respectively. This indicates that the distribution of separations between the first two planets is different than between the second and third and other outer pairs of planets in these systems.

As also discussed by CT14, the generally larger values of \( \phi_{\Delta r,1} \) may be a signature of the greater relative effect of inner disk clearing after first, Vulcan planet formation on the location
**Figure 8.** Same as Figure 7, but now showing absolute values of mass surface density (top row) and midplane pressure (bottom row) of disks with a $0.5M_\odot$ planet with (left column) fixed $\alpha$ profile (after 1000 orbits) and (right column) evolving $\alpha$ profile (Case A, after 7000 orbits).

**Figure 9.** Same as the top row of Figure 8, but now showing a spatial map of the disk structure induced by a $0.5M_\odot$ planet with (left) fixed $\alpha$ profile (after 1000 orbits) and (right) evolving $\alpha$ profile (Case A, after 7000 orbits).
of the second planet, compared to later, more incremental dead zone retreats.

7. SUMMARY AND DISCUSSION

We have explored three main aspects of the IOPF scenario with numerical simulations of planet–disk interactions. Our main findings are the following:

1. Planets of all relevant masses are trapped at the DZIB transition region, so planetary migration (of Type I or Type II) does not appear to be a problem for IOPF. Especially during the early stages of potential Type I migration, the fact that the protoplanet is trapped at its formation location should allow it to continue to accrete, especially by pebble accretion.

2. The mass scale of significant gap opening that can affect pebble accretion by displacing the local pressure maximum away from the planet is $M_p \approx 0.5 M_G$, i.e., $\phi_G \approx 0.5$, which is about 6 $M_e$ in the fiducial case at $r = 0.1$ AU. This is similar to the fiducial value adopted by CT14, especially since, given the renormalization of $M_G$ by a factor of 0.745 in this paper (Section 2), this means that the overall change in planet mass is only a factor of 1.24. However, these results are derived in the context of pure hydrodynamic simulations and may be sensitive to including extra physics of MRI activation in the gap region.

3. A simple model for MRI activation in the gap region, implemented by an evolving $\alpha$ viscosity profile set by X-ray penetration, leads to greater retreat of the pressure maximum out to separations of ~20–70 Hill radii of the planet, but sensitive to model assumptions about the shape of the viscosity profile in the MRI-active region to dead zone transition region. Such separations overlap with the observed orbital separations of innermost planets in STIPs. Future work is needed to better model viscosity profiles in such transition regions.

While the above results are supportive of the IOPF model for being relevant for formation of STIPs, a number of open questions remain. For example, even though planets with masses $\geq 0.1 M_G$ appear likely to be trapped at a location where they can continue to grow by pebble accretion, it is possible that this is not the case at earlier stages for lower-mass protoplanets. Faure et al. (2015) have pointed out that inwardly migrating vortices can form at the dead zone inner edge and can potentially interact with the planet, possibly causing it to also migrate inward. However, their 3D simulation results are for an unstratified disk, and the mass accretion rate is not a constant across the dead zone inner edge, leading to mass pileup and potentially influencing vortex formation. The potential effects of vortex interactions still need to be confirmed in 3D stratified simulations where the presence of the surface active layer may transport the disk mass smoothly across the dead zone inner edge. In our 2D simulations, we used a small viscosity in the dead zone region to represent the effects of an active layer and/or turbulent wakes spreading from the inner MRI-active region, which may control the accretion rate in this radial region of the disk. With this setup we do not observe the sharp density peaks at the dead zone.

Figure 10. Comparison of orbital separations of the Kepler-ddetected planets (see legend) and our simulation results for DZIB pressure maximum retreat: vertical long-dashed line shows $\phi_{\Delta r, P_{max}} = 4.75$ for the initial gap opening in the fixed $\alpha$ profile disk. The three short-dashed lines show the estimated values of $\phi_{\Delta r, P_{max}} = 25.3, 56.3, 67.6$ for Cases A, B, C, respectively, of the evolving $\alpha$ profile disk.
inner edge that were present in the Faure et al. (2015) simulations.

Further work is needed on the IOPF model to study the transition of the pebble ring to a single dominant protoplanet, potentially involving streaming and gravitational instabilities of the pebble population and/or Rossby wave instabilities in the gas, followed by oligarchic growth of planetesimals combined with continued pebble accretion. Improved study of pebble supply truncation during the process of gap opening, including utilizing 3D simulations (see Lambrechts et al. 2014, e.g., calculations focused on the outer disk), is also needed.

Potential migration of planets after their main accretion phase and retreat of their natal DZIB, including that due to interactions between neighboring planets, is another topic for future study. However, we note that for the fiducial IOPF model, the gas mass that is present in the vicinity of the first planet to form is relatively small compared to the planet’s mass, thus limiting the scope of its migration.

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APPENDIX
DERIVATION OF DISK PROPERTIES

Here we update the analysis presented in CT14, which involves modest changes in disk properties, as discussed in Section 2. Conservation of angular momentum in a viscous disk implies

\[ r \frac{\partial}{\partial r} \left( \Sigma_g r^2 \Omega \right) + \frac{\partial}{\partial r} \left( r \Sigma_g r^2 \Omega v_r \right) = \frac{1}{2\pi} \frac{\partial \Gamma}{\partial r}, \tag{10} \]

where \( \Gamma(r, t) \) is the shear torque from viscosity,

\[ \Gamma(r, t) = 2\pi \nu \Sigma_g r^3 \frac{d\Omega}{dr}. \tag{11} \]

In a steady disk, we have \( \frac{\partial}{\partial t} \left( \Sigma_g r^2 \Omega \right) = 0 \), so integrating Equation (10), we obtain

\[ r \Sigma_g r^2 \Omega v_r = \frac{\Gamma}{2\pi} + C. \tag{12} \]

Substituting \( \Gamma(r, t) \), we obtain

\[ \nu \Sigma_g \frac{d\Omega}{dr} + \frac{C}{r^3} = \Sigma_g \Omega v_r. \tag{13} \]

The boundary condition at \( r = r_g + \delta r \) \( \frac{d\Omega}{dr} = 0 \), so constant \( C \) is

\[ C = r \Sigma_g \Omega \left( r_g + \delta r \right) = -\dot{m} \left( \frac{Gm_*}{r_g} \right)^{1/2} / (2\pi), \tag{14} \]

where

\[ \dot{m} = 2\pi r \Sigma_g (-v_r). \tag{15} \]

For \( \delta r \ll r_g \), we have \( \Omega(r_g + \delta r) \approx \Omega(r_g) \left( \frac{r_g}{r} \right)^{1/2} \), and substituting into Equation (13), we have

\[ \nu \Sigma_g = \frac{\dot{m}}{3\pi} \left[ 1 - \left( \frac{r_g}{r} \right)^{1/2} \right]. \tag{16} \]

So the energy dissipation rate per unit area (only via one face of the disk) at radius \( r \) is

\[ D(r) = \frac{\Gamma (d\Omega/dr)}{4\pi r} = \frac{\nu \Sigma_g r^2}{2} \left( \frac{d\Omega}{dr} \right)^2 = \frac{3Gm_* \dot{m}}{8\pi r^3} \left[ 1 - \left( \frac{r_g}{r} \right)^{1/2} \right]. \tag{17} \]

From the midplane to disk surface, the optical depth is

\[ \tau_{\text{tot}} = 0.5 \Sigma_g \kappa. \tag{18} \]

From Equation (3.11) in Hubeny (1990), we know the relation between surface temperature and actual temperature where the optical depth is \( \tau \) to the surface of the disk:

\[ T^4(\tau) = \frac{3}{4} T_{\text{eff}}^4 \left( 1 - \frac{\tau}{2\tau_{\text{tot}}} \right) = \frac{3}{4} T_{\text{eff}}^4 \tau_{\text{tot}}. \tag{19} \]

Here \( \tau_{\text{tot}} = 0.5 \Sigma_g \kappa \), and in our situation, \( D(r) = \sigma T_{\text{eff}}^4 \), \( T_c = T(\tau_{\text{tot}}) \), so

\[ \frac{16\sigma}{3\Sigma \kappa} T_{\text{eff}}^4 T_c^4 = D(r). \tag{20} \]

We have an expression for midplane temperature:

\[ T_c^4 = \frac{9Gm_* \dot{m} \Sigma_g \kappa}{128\pi \sigma r^3 \kappa} \left[ 1 - \left( \frac{r_g}{r} \right)^{1/2} \right] r^{-3/2}. \tag{21} \]

but we still have an unknown \( \Sigma \) profile, so now we try to deduce it. In an \( \alpha \) disk, we have

\[ \nu = \alpha \frac{c_s^2}{\omega_k}. \tag{22} \]

Substituting in Equation (16), we obtain

\[ \Sigma_g = \frac{\dot{m} \sqrt{Gm_*}}{3\pi \alpha c_s^2} \left[ 1 - \left( \frac{r_g}{r} \right)^{1/2} \right] r^{-3/2}. \tag{23} \]

For an adiabatic sound speed \( c_s \), we have

\[ c_s^2 = \frac{dP}{d\rho} = \gamma \frac{P}{\rho}. \tag{24} \]

Then the midplane pressure satisfies

\[ P = \frac{\rho k T_c}{\mu} + \frac{4\sigma}{3c} T_c^4 \approx \frac{\rho k T_c}{\mu}. \tag{25} \]

Now we have the following relation between \( \Sigma_g \), \( r \), and \( T_c \):

\[ \Sigma_g = \frac{\dot{m} \sqrt{Gm_*}}{3\pi \alpha} \frac{\mu}{\gamma k T_c} \left[ 1 - \left( \frac{r_g}{r} \right)^{1/2} \right] r^{-3/2}, \tag{26} \]
so, substituting for $T_c(r)$ from Equation (21), the surface density profile is
\[
\Sigma_g = \frac{2^{7/5}}{3^{6/5} \pi^{3/5}} \left( \frac{\mu}{\gamma k_B} \right)^{4/5} \left( \frac{\kappa}{\sigma_{SB}} \right)^{-1/5} \\
\times \alpha^{-2/5} \left( Gm_s \right)^{1/5} \left( f, m \right)^{3/5} r^{-3/5},
\]  
and midplane temperature (here we use $T$ instead of $T_c$) is
\[
T = \frac{3^{1/5}}{2^{1/5} \pi^{-2/5}} \left( \frac{\mu}{\gamma k_B} \right)^{1/5} \left( \frac{\kappa}{\sigma_{SB}} \right)^{1/5} \\
\times \alpha^{-5/6} \left( Gm_s \right)^{3/10} \left( f, m \right)^{2/5} r^{-9/10}.
\]  
To calculate scale height $h$, usually it is assumed that the disk is vertically isothermal in a passive disk, here in an active disk, we use an adiabatic vertical structure:
\[
\frac{h}{r} = \frac{c_s}{v_\phi} = \frac{c_l}{v_K} = \frac{c_l}{\sqrt{Gm_s/r}},
\]
so the aspect ratio is
\[
\frac{h}{r} = \frac{3^{1/10}}{2^{1/10} \pi^{-1/5}} \left( \frac{\mu}{\gamma k_B} \right)^{-2/5} \left( \frac{\kappa}{\sigma_{SB}} \right)^{1/10} \\
\times \alpha^{-1/10} \left( Gm_s \right)^{-7/20} \left( f, m \right)^{1/5} r^{1/20}.
\]  
Since the disk vertical structure satisfies $\rho(z) = \rho(z = 0)e^{-z^2/2h^2}$, midplane density $\rho = \Sigma_g/\sqrt{2\pi h}$ can be expressed as
\[
\rho = \frac{2^{8/5}}{3^{13/10} \pi^{9/10}} \left( \frac{\mu}{\gamma k_B} \right)^{6/5} \left( \frac{\kappa}{\sigma_{SB}} \right)^{-3/10} \\
\times \alpha^{-7/10} \left( Gm_s \right)^{11/20} \left( f, m \right)^{2/5} r^{-33/20}.
\]  

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