GPS/INS Integrated Navigation System for Autonomous Robot

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ABSTRACT

Nowadays, autonomous robots are capable of replacing people with hard work or in dangerous environments, so this field is rapidly developing. One of the most important tasks in controlling these robots is to determine its current position. The Global Positioning System (GPS) was originally developed for military purposes but is now widely used for civilian purposes such as mapping, navigation for land vehicles, marine, etc. However, GPS has some disadvantages like the update rate is low or sometimes the satellites’ signal is suspended. Another navigation system is the Inertial Navigation System (INS) can allow you to determine position, velocity and attitude from the subject’s status, like acceleration and rotation rate. Essentially, INS is a dead-reckoning system so it has a huge cumulative error. An effective method is to integrate GPS with INS, in which the center is a nonlinear estimator (e.g. the Extended Kalman filter) to determine the navigation error, from which it can update the position the object more accurately. To improve even better accuracy, this paper proposes new method which combines the original integrated GPS/INS with tri-axis rotation angles estimation and velocity constraints. The experimental system is built on a low-cost IMU with tri-axis gyroscope, accelerometer and magnetometer and a GPS module to verify the model algorithm. Experiment results have shown that the rotation angles estimator helps us to determine the Euler angles correctly, thereby increasing the quality of the position and velocity estimation. In practice, the accuracy of roll and pitch angle is 2 degrees, the error of yaw angle is still large. The achieved horizontal accuracy is 2m when the GPS signal is stable and 3m when the GPS signal is lost in a short period. Compared with individual GPS, the error of the integrated system is about 10% smaller.

Key words: Autonomous Robot, GPS/INS Integration, IMU

INTRODUCTION

For autonomous robots (such as USV, UAV, AUV, etc.) to work in a stable and efficient manner, navigation is one of the most important issues to be aware of. The Global Positioning System (GPS) was originally developed for military purposes but is now widely used for civilian purposes such as mapping, navigation for land vehicles, marine, etc. However, GPS has some disadvantages like the update rate is low or sometimes the satellites’ signal is suspended. Another navigation system is the Inertial Navigation System (INS) can allow you to determine position, velocity and attitude from the subject’s status, like acceleration and rotation rate. Essentially, INS is a dead-reckoning system so it has a huge cumulative error. An effective method is to integrate GPS with INS, in which the center is a nonlinear estimator (e.g. the Extended Kalman filter) to determine the navigation error, from which it can update the position the object more accurately.

Depending on the “depth” of the interaction and for the shared information between the GPS and INS, we have some integration methods: uncoupled integration, loosely coupled (LC), tightly coupled (TC) and deeply integrated². For uncoupled method, GPS output is used as the “reset” signal for the INS. When there is no GPS solution (position and velocity), the integrated system uses INS to estimate. This method has the simplest structure, but the system cannot estimate the sensor’s drift, so it is not commonly used. In LC method, GPS solutions will be compared with the inertial estimation in order to calculate the error state of the object. In TC method the integration is “deeper”; the raw measurements of the GPS (pseudo-range and Doppler measurements) are directly combined with the calculated INS estimation results in an appropriate filter. Both LC and TC systems operate in closed loop, i.e. position, velocity, attitude errors and sensor’s drifts are fed back for the INS and GPS to make a navigation correction. The loosely coupled model is simpler than the tightly one. The structure of tightly coupled model and deeply integration are very complex, so we do not mention in this paper.

In estimating Euler angles, conventional INS systems use tri-axis angular rate to calculate these angles. However, MEMS (Micro-Electro-Mechanical Systems) have some limitations, especially in long-term stability. Therefore, it is important to develop a new method which combines the original integrated GPS/INS with tri-axis rotation angles estimation and velocity constraints.
Inertial navigation system

INS is a navigation system that uses tri-axis inertial sensors (gyroscope, accelerometer and magnetometer) to calculate the orientation and position of an object. This system does not need an external reference, so it can continuously calculate without interruption. In this paper, outputs of inertial sensors are three components of the gyroscope, three components of the accelerometer and three components of the magnetometer in the body-frame, denoted by $\omega^b$, $\mathbf{f}^b$, $\mathbf{m}^b$ respectively. The Figure 1 describes the INS mechanization in NED frame. The INS uses rotation rate and acceleration values from the IMU sensor to update attitude, velocity and position by the following formula:

\[
\begin{bmatrix}
\mathbf{r}^n \\
\mathbf{v}^n \\
\mathbf{C}^n_b
\end{bmatrix} =
\begin{bmatrix}
1 & -\omega_{bn}^n & \omega_{bn}^n \\
\omega_{bn}^n & 1 & -\omega_{bn}^n \\
-\omega_{bn}^n & \omega_{bn}^n & 1
\end{bmatrix}
\begin{bmatrix}
\mathbf{f}^b \\
\omega^b \\
\mathbf{m}^b
\end{bmatrix} +
\begin{bmatrix}
\mathbf{g}^n \\
\mathbf{0} \\
\mathbf{0}
\end{bmatrix}
\]

In this formula, vector $\mathbf{r}^n = [\varphi \hspace{1mm} \lambda \hspace{1mm} h]^T$ is the position vector, whose components are geographic latitude, longitude and altitude (height) respectively. Vector $\mathbf{v}^n$ is the velocity vector in NED coordinate. Matrix $\mathbf{C}^n_b$ is the position vector, whose components are geographic latitude, longitude and altitude (height) respectively. Vector $\mathbf{v}^n$ is the velocity vector in NED coordinate. Matrix $\mathbf{C}^n_b$ is the direction cosine matrix (DCM, or rotation matrix) from body-frame to NED frame. The symbols $\omega$ and $\Omega$ denote the angular rate and its skew symmetric form, matrix $\mathbf{D}$ is the transition matrix from NED frame to latitude, longitude and altitude:

\[
\mathbf{D} =
\begin{bmatrix}
M + h & 0 & 0 \\
0 & (N + h) \cos \varphi & 0 \\
0 & 0 & -1
\end{bmatrix}
\]

Formula (1) is written in continuous form. In experiment, we have to discretize it for simplicity in calculation. Because of this discretization, the update process always has error. On the other hand, IMU sensor has other types of error like bias and scale factor. Thus, the INS errors are rapidly accumulating. To improve the accuracy of the navigation estimation, we use a tri-axis Euler angles estimator. It is structured as a two-stage cascaded Extended Kalman filter (Figure 2). These filters use acceleration and magnetic field measured from the IMU to correct the Euler angles (roll, pitch and yaw). Precisely, first the EKF-1 combines the gyroscope and accelerometer measurements to calculate the Earth’s gravity vector in NED frame, and then it can determine roll and pitch angles. Next, the EKF-2 uses the gyroscope, magnetic field measurements and the determined roll and pitch to calculate yaw angle. In experimental conditions, the accuracy of roll and pitch is 1 degree and accuracy of yaw angle is 3 degrees.

Rotation rate and acceleration measurements can be affected by noises such as deviation, scale factor, non-orthogonality and some other types. Some types of error can be identified and calibrated in the laboratory environment. Some types are unpredictable, and...
have to be modeled as random noise. In the above factors, bias has the greatest effect on the measurement value of the IMU. So we can model the remaining types of noise (except bias) as white noise (denoted by the symbol $\eta$), we have the estimation equation:

$$\begin{align*}
\dot{f} &= \dot{f} - b_a + \eta_a \\
\dot{\omega} &= \dot{\omega} - b_g + \eta_g
\end{align*}$$

(3)

In (3), the symbols $\dot{f}$ and $\dot{\omega}$ are estimated values of acceleration and angular velocity, $\dot{f}$ and $\dot{\omega}$ are values measured from the IMU sensor, the symbol $b$ is the bias and $\eta$ is the other types of noise (modeled as white noise).

**Loosely Coupled scheme**

The loosely coupled model also referred to as “decentralized” filtering, consists of two estimators. The first one is a nonlinear estimator. It combines the INS estimation results with the GPS results to estimate the position, velocity, attitude error and the IMU sensor’s error. The second is the GPS filter. It uses the pseudorange and Doppler measurement values from GPS module to determine the position, velocity. Figure 3 shows the diagram of loosely coupled model.

In today’s GPS modules, there is usually a built-in GPS data processor, which can calculate position, velocity and some other information from GPS raw data. In the LC model, position and velocity are fed into the nonlinear filter. The filter used in this paper is the Extended Kalman filter, which is suitable for nonlinear systems. Measurement values from IMU sensor (angular rate and acceleration) after being computed using the Euler angles estimation and INS mechanization, will be compared with the position and velocity of the GPS. The difference between two results is used as the input of the EKF. The integrated system works in closed loop, the estimated error values are fed back to adjust the state of the INS system and to compensate for the IMU measurements. This close-loop model is suitable for MEMS IMU, which has large disturbance.

The error state vector $\delta x$ of the EKF filter in this model is composed of the position error $\delta r^m$, the velocity error $\delta v^m$, the attitude error $\dot{\epsilon}$, the acceleration bias error $\delta b_a$, and the gyroscope bias error $\delta b_g$. Derive the INS mechanization function and take the first order elements, we have the process model equation:

$$\delta x = F \delta x + G u \quad (4)$$

where:

$$F = \begin{bmatrix}
F_{rr} & F_{rv} & 0_{3x3} & 0_{3x3} & 0_{3x3} \\
F_{rv} & F_{vv} & (f^m x) & C^m_{b} & 0_{3x3} \\
0_{3x3} & 0_{3x3} & -C^m_{b} & -C^m_{b} & 0_{3x3} \\
0_{3x3} & 0_{3x3} & 0_{3x3} & -1/\tau_{ba} & 0_{3x3} \\
0_{3x3} & 0_{3x3} & 0_{3x3} & 0_{3x3} & -1/\tau_{bg}
\end{bmatrix}$$

$$G = \begin{bmatrix}
0_{3x3} & 0_{3x3} & 0_{3x3} & 0_{3x3} \\
C^m_{b} & 0_{3x3} & 0_{3x3} & 0_{3x3} \\
0_{3x3} & -C^m_{b} & 0_{3x3} & 0_{3x3} \\
0_{3x3} & 0_{3x3} & 0_{3x3} & 0_{3x3} \\
0_{3x3} & 0_{3x3} & 0_{3x3} & 0_{3x3}
\end{bmatrix} \quad (6)$$

In matrix $F$, $\tau_{ba}$ and $\tau_{bg}$ are the correlation time vectors of accelerometers and gyroscopes, determined based on the Gauss-Markov model. The components of vector $u$ are white noises, with the covariance determined by the formula:

$$Q = \text{diag} \left( \begin{bmatrix} q_a & q_g & q_{ba} & q_{bg} \end{bmatrix} \right), \quad q = \frac{2\sigma^2}{\tau}
$$

In the above formula, $\sigma$ is the standard deviation of the Gauss-Markov noise. Matrix $Q$ is called the spectral density matrix and its component, respectively, are covariance accelerometer, gyroscope, accelerometer bias and gyroscope bias. These values can be determined in the datasheet of the sensor.

The measurement model of the EKF is the difference of the INS results (position and velocity) and GPS results:

$$\delta z = \begin{bmatrix}
\gamma^r_{\text{INS}} - \gamma^r_{\text{GPS}} \\
\gamma^v_{\text{INS}} - \gamma^v_{\text{GPS}}
\end{bmatrix} = H \delta x + \epsilon \quad (8)$$

In the above equation, symbol $\epsilon$ is the measurement noise. Its covariance matrix $R$ can be obtained from GPS processing. The activation of the EKF is divided into 2 stages: update and prediction. The Kalman gain is computed first in the update stage. Then state variables ($\delta x$) and error covariance ($P$) are updated based on prior estimates and its error covariance. After each correction, the error state vector should be reset to zero.

When there is a GPS outage, we can use velocity constraints (Figure 4) to estimate errors. In simulation, we use FlightGear simulation software to create the data file and use MATLAB/Simulink to process it. The GPS signal is disturbed with noise to research about noise suppression of the estimator. The standard deviation of noise is 2.5 m in each horizontal axis and 5 m in vertical axis. Simulations were made in two cases: with and without the Euler angles estimator. We have the result Table 1:

From the above table, we can see that with the rotation angles estimator, the results are better. The horizontal
accuracy is about 0.64 meters. The velocity error is within 0.1 m/s. We can conclude that the estimator has good filtering capability. Next, we will examine the quality of the system when the GPS signal is lost in intervals of 3, 5 and 10 seconds.

From Table 2, we can conclude that when there is a GPS outage, the error of the system will be larger than the normal case (GPS fix). In addition, if the GPS lost time is longer, the horizontal error is larger. Using an Euler angles estimator helps to make smaller errors.

EXPERIMENTAL RESULTS AND DISCUSSION

Hardware development

We built an experimental system to verify the implemented algorithm. The hardware (Figure 5) consists of the IMU sensor ADIS16405 from Analog Devices, the GPS module from U-blox and the microcontroller STM32F407 (ARM Cortex-M4) from STMicroelectronics. The reference system is the GNSS/INS system from Xsens Technology. The MTi-G-700 can give rotation angles estimate with a 1 degree accuracy, position error of 2 meters and velocity error of 0.05 m/s. The update rate of INS and GPS are 100 Hz and 10 Hz, respectively. In each INS cycle of 10 milliseconds, the STM32F407 microcontroller reads data from the IMU sensor and the GPS module. Then update the error estimator, using Extended Kalman filter algorithm. Navigation data is sent to the computer via COM/RS232 port or via SD card.

Results

For MEMS IMU sensors, the amplitude of its noise is huge, so if we do not use the Euler angles estimator, the result is bad, the attitude, position, velocity errors are enormous. The estimated trajectory (red dots in Figure 6) does not have the same shape with the reference one (black line). In contrast, when we use the angles estimator, the errors are smaller, the accuracy is higher. The horizontal error of our GPS/INS system is 1.69 m, while the error of the individual GPS system is 1.93 m. For this reason, the GPS/INS algorithm can reduce over 10% of the error. On the other hand, the update rate of GPS is only 10 Hz. The integrated GPS/INS update rate is 10 times larger (100 Hz). We can see the effective of high update rate in Figure 6. Because the GPS has the low update rate of 10 Hz, there are visible spaces between the green dots (GPS-only). And if the vehicle moves very fast, the GPS cannot describe the vehicle’s trajectory accurately. Differently, the blue dots (GPS/INS) approx

Table 1: Attitude, position and velocity errors

| Error            | Without Euler angles estimation | With Euler angles estimation |
|------------------|---------------------------------|------------------------------|
| Attitude (r-p-y) (degree) | 24.7  48.6  14.8 | 2.0  2.0  2.0 |
| Position NED (m)  | 0.69   1.54  1.62 | 0.43  0.47  2.99 |
| Velocity NED (m/s)| 1.80   3.46  4.61 | 0.05  0.05  0.04 |
Table 2: Horizontal accuracy during GPS outages

| GPS outage | Without Euler angles estimation | With Euler angles estimation |
|------------|---------------------------------|-----------------------------|
| 3 seconds  | 15.0 m                          | 0.88 m                      |
| 5 seconds  | 35.8 m                          | 0.92 m                      |
| 10 seconds | 171.4 m                         | 1.33 m                      |

Figure 4: EKF with velocity constraints.

Table 3: Attitude, position and velocity errors

| Error               | Without Euler angles estimation | With Euler angles estimation |
|---------------------|---------------------------------|-----------------------------|
| Attitude (r-p-y)    | 70                              | 83                          |
| (degree)            | 29                              | 1.31                        |
| 16.7                | 1.07                            |
| Position NED (m)    | 11                              | 313                         |
|                     | 7.7                             | 1.58                        |
|                     | 3.42                            |
| Velocity NED (m/s)  | 10                              | 85                          |
|                     | 6.4                             | 0.27                        |
|                     | 0.46                            |
approximately form a continuous line. From the above results, it can be concluded that the angles estimator can improve the accuracy of the navigation system and the integrated GPS/INS system performs better than the single GPS system (Table 3).

Next, assuming the GPS signal is lost for a period of 5 seconds, we will analyze the accuracy of implemented GPS/INS system in cases with and without speed constraints. We will simulate GPS outages in two cases: GPS lost in straight line and in curved line (Table 4). From the above results, we can see in the normal case of GPS fix, the velocity constraints can still reduce the horizontal error of the system. When there is a GPS outage, using speed constraints can either increase or decrease the system's accuracy. However, it restricts the trajectory from divergence. The blue dots in Figures 7 and 8 can follow the reference trajectory, while the red dots are diverging. Thus, velocity constraints are also a tool that can improve the accuracy of the integrated GPS/INS navigation system.

**CONCLUSIONS**

In this paper, we have implemented a loosely coupled GPS/INS integrated navigation system. The main algorithm in this system is the Extended Kalman filter. We combined the EKF with Euler angles estimator and velocity constraints to improve accuracy.

The rotation angles estimator helps us to determine the Euler angles correctly, thereby increasing the quality of the position and velocity estimation. In practice, the accuracy of roll and pitch angle is 2 degrees, the error of yaw angle is still large.

The achieved horizontal accuracy is 2m when the GPS signal is stable and 3m when the GPS signal is lost in a short period. Compared with individual GPS, the error of the integrated system is about 10% smaller. In addition, the positive point of the GPS/INS is its update rate reaches 100 Hz, which is 10 times larger than the initial system. When there is a long-period GPS outage, the LC algorithm's result is very bad, so we need to use the tightly coupled model. In the future, we will research about this model, point out its advantages and disadvantages, and compare with the original model. After that, we will find the optimal switching method between two models.
Table 4: Horizontal accuracy when GPS lost, with and without velocity constraints

| Horizontal error (m) | GPS fix | 5 seconds GPS lost, straight line | 5 seconds GPS lost, curved line |
|----------------------|---------|----------------------------------|--------------------------------|
| Without velocity constraints | 1.69 | 2.23 | 2.60 |
| With velocity constraints | 1.59 | 2.76 | 1.96 |

Figure 7: GPS outage – straight line.

Figure 8: GPS outage – Curved line.
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CONFLICT OF INTERESTS

The author declares that this paper has no conflict of interests.

AUTHORS’ CONTRIBUTIONS

Tran Ngoc Huy has developed the proposed algorithm and wrote the manuscript. Le Manh Cam and Nguyen Thanh Nam implemented simulation, experiment and wrote the manuscript.

ABBREVIATIONS

USV: Unmanned Surface Vehicle
UAV: Unmanned Aerial Vehicle
AUV: Autonomous Underwater Vehicle
GPS: Global Positioning System
INS: Inertial Navigation System
LC: Loosely Coupled
TC: Tightly Coupled
EKF: Extended Kalman Filter

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Xây dựng hệ thống định vị tích hợp GPS/INS cho robot tự hành

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TÓM TÁT

Các loại robot tự hành có khả năng thay thế con người làm những công việc nặng nhọc, ở những môi trường khó khăn, nguy hiểm, vì vậy lĩnh vực này hiện đang rất phát triển. Một trong những vấn đề quan trọng trong việc điều khiển các loại robot tự hành đó là xác định vị trí hiện tại của robot. Hệ thống định vị toàn cầu (GPS) được sử dụng rộng rãi trong lĩnh vực này, tuy nhiên có một số nhược điểm như tốc độ cập nhật thấp hoặc mất tín hiệu từ các vệ tinh. Một hệ thống điều hướng khác là Hệ thống dẫn đường quán tính (INS) có thể cho phép ta xác định vị trí, vận tốc và góc xoay của robot. Tuy nhiên, INS khi tính toán sẽ làm sai số tích lũy theo thời gian. Một phương pháp hiệu quả là tích hợp GPS với INS, trong đó quá trình của hệ thống là cộng với định lượng của Hệ thống GPS và INS so với khi tích hợp riêng rẽ. Bài báo này giới thiệu về phương pháp tích hợp lỏng GPS/INS, sử dụng bộ ước lượng góc xoay ba trục và ràng buộc vận tốc để cải thiện độ chính xác. Giải thuật được thực nghiệm kiểm chứng trên cảm biến quán tính gồm cảm biến quay hồi chuyển, cảm biến gia tốc, tử tự giữa bauve và cảm biến GPS. Kết quả cho thấy sai số của góc roll và pitch là 2 độ, sai số của góc yaw rộng hơn. Độ chính xác theo phương ngang đạt được là 2m khi tín hiệu GPS ổn định và 3m khi tín hiệu GPS bị mất trong một khoảng thời gian ngắn. So với hệ thống GPS riêng lẻ, sai số của hệ thống tích hợp nhỏ hơn khoảng 10%.

Từ khoá: Robot tự hành, Tích hợp định vị/hệ thống định vị quán tính