COSMIFLOWS-2: I-BAND LUMINOSITY–H\(_1\) LINEWIDTH CALIBRATION

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ABSTRACT

In order to measure distances with minimal systematics using the correlation between galaxy luminosities and rotation rates it is necessary to adhere to a strict and tested recipe. We now derive a measure of rotation from a new characterization of the width of a neutral hydrogen line profile. Additionally, new photometry and zero-point calibration data are available. Particularly the introduction of a new linewidth parameter necessitates the reconstruction and absolute calibration of the luminosity–linewidth template. The slope of the new template is set by 267 galaxies in 13 clusters. The zero point is set by 36 galaxies with Cepheid or tip of the red giant branch distances. Tentatively, we determine \(H_0 \sim 75\) km s\(^{-1}\) Mpc\(^{-1}\). Distances determined using the luminosity–linewidth calibration will contribute to the distance compendium Cosmicflows-2.

Key words: distance scale – galaxies: distances and redshifts – galaxies: photometry – radio lines: galaxies

Online-only material: color figures

1. INTRODUCTION

Cosmicflows-1 is the re-christened name of the catalog of galaxy distances published by Tully et al. (2008) and available at the Extragalactic Distance Database (EDD).\(^3\) That catalog contains distance measures for 1797 galaxies, in the majority from the correlation between galaxy luminosity and rotation rate (Tully & Fisher 1977) but also including Cepheid period–luminosity relation (Freedman et al. 2001), tip of the red giant branch (Rizzi et al. 2007; Jacobs et al. 2009), and surface brightness fluctuation (Tonry et al. 2001) distance estimates. Cosmicflows-1 is quite limited in depth, extending to only 3000 km s\(^{-1}\). However, it provides the densest coverage of the historical Local Supercluster of any available catalog.

Cosmicflows-2 is a catalog in construction that will build on the high density of local coverage but will also extend to considerably greater distances. In addition to an update of the Cepheid, red giant branch, and surface brightness fluctuation information the new catalog will include Type Ia supernova (Jha et al. 2007) and fundamental plane (Colless et al. 2001; Hudson et al. 2001; Bernardi et al. 2002) material. However, once again, the numerically dominant source of distances will come from the luminosity–H\(_1\) linewidth correlation. Courtois et al. (2011b) have described several luminosity–linewidth samples that will be major components of Cosmicflows-2. The purpose of the present paper is to provide a new calibration of the luminosity–linewidth correlation.

The calibration of this correlation used with Cosmicflows-1 was described in detail by Tully & Pierce (2000), with minor updates in Tully et al. (2008). The linewidth measure used with those earlier discussions is \(W_{20}\), the width of an H\(_1\) profile at 20% of peak intensity. This is an analog measure with origins that date back to the first paper by Tully & Fisher. As we move forward with digital data and incorporate larger samples it is an appropriate moment to reconsider the details of the measurement of a profile width. The new profile measure that we choose is different enough that it imposes the need for a new end-to-end re-calibration of the methodology.

While the recent influx of high quality digital H\(_1\) profile information is the largest driver for this re-calibration, there is considerably more photometric material available today and more galaxies are available with accurate Cepheid or tip of the red giant branch distance determinations that can establish the scale zero point. This combination of advances motivates the re-calibration to be discussed as a prelude to the publication of Cosmicflows-2.

2. CALIBRATOR SAMPLE

The calibration of the luminosity–linewidth correlation involves two important steps: the first with the establishment of the slope of the correlation that is critical for the minimization of a form of Malmquist bias and the second with the establishment of the scale zero point. The slope of the correlation is given through an analysis of samples drawn from clusters of galaxies. The details of the choice of clusters are discussed in Section 4 and the elaboration is given in the Appendix. In the present study the correlation slope is given by data from 267 galaxies drawn from 13 clusters, compared with 241 galaxies drawn from 12 clusters used earlier (Tully & Pierce 2000).

With the slope fixed, the scale zero point is established from the luminosity–linewidth properties of relatively nearby galaxies with independently determined distances. This problem is discussed in Section 5. Presently the scale zero point is set by 36 galaxies with well determined Cepheid period–luminosity (Freedman et al. 2001) or tip of the red giant branch (Rizzi et al. 2007) distance measures, compared with 24 available earlier.

Implementation of the luminosity–linewidth methodology requires the observation of three parameters: (1) a measure of the rotation rate obtained by observing the width of the 21 cm H\(_1\) spectral line; (2) the apparent luminosity of the galaxy, in this case represented by the flux in the near-infrared I band; and (3) the inclination of the galaxy, inferred from the ellipticity of the photometric image, and used to de-project the measure of rotation to what would be seen in an edge-on view and to de-project reddening to what would be seen in a face-on view. The relevant data are being accumulated for the large Cosmicflows-2 sample. The following two subsections

\(^3\) http://edd.ifa.hawaii.edu
summarize the transformation steps from raw observables to parameters used in fitting for distances.

2.1. \( H I \) Linewidths

Major radio observatories have preserved digital \( H I \) spectral flux data from observations extending back more than two decades. We have gathered over 12,000 profiles from these archival sources and complemented them with some 2000 profiles from our own recent observations. The task we then undertook was to analyze all this material in a consistent way.

An \( H I \) profile linewidth that we might measure is a utilitarian parameter only indirectly connected with the physics of galactic rotation. Several alternative linewidth definitions were explored by Springob et al. (2005). We have settled on a variant of one of these. The justifications and details of our preferred linewidth measure are given by Courtois et al. (2009, 2011b). In brief, we want a measure with the following properties: (1) at a level low enough to capture the full range of rotation motions while high enough to usually be above noise and wings in profiles that are adequately observed and (2) not sensitive to details of the profile shape, i.e., whether the profile is single or double peaked or whether the flux in peaks is asymmetric. The measured parameter is \( W_{50,m} \), the linewidth at 50% of the mean flux per channel contained within spectral channels embracing 90% of the total flux. Width error estimates are based on the level of the signal, \( S \), at 50% of mean flux over the noise, \( N \), measured beyond the extremities of the signal (Courtois et al. 2009).

Useful profiles have error estimates no greater than 20 km s\(^{-1}\) corresponding to a flux per channel \( \frac{S}{N} \geq 2 \). This minimum \( S/N \) level corresponds approximately to a peak signal-to-noise ratio of 7.

It was described by Courtois et al. that the linewidth parameter must be corrected for redshift and instrumental broadening

\[
W_{c,m}^{e} = W_{50,m}^{e} - 2\Delta \nu \lambda, \tag{1}
\]

where \( c_{z} \) is the heliocentric velocity of the galaxy, \( \Delta \nu \) is the spectral resolution after smoothing, and \( \lambda = 0.25 \) is determined empirically. There was further discussion that this utilitarian parameter could be transformed into an approximation to a physically meaningful parameter: the velocity difference between the positive and negative extremes of rotation in the galaxy. The physically motivated parameter is \( W_{m}^{e} \):

\[
W_{m}^{2} = W_{m}^{2} + W_{c,m}^{e 2} [1 - 2 e^{-(W_{m}^{e}/W_{c,m}^{e})^2}] - 2W_{m}W_{c,m}^{e 2} [1 - e^{-(W_{m}^{e}/W_{c,m}^{e})^2}], \tag{2}
\]

with \( W_{c,m}^{e} = 100 \text{ km s}^{-1} \) descriptive of the transition from boxcar to Gaussian profile shapes and \( W_{c,50}^{e} = 9 \text{ km s}^{-1} \) a parameter determined by random internal motions. Finally, a projection correction is made with \( W_{m}^{e} = W_{m}^{e} / \sin(i) \) where \( i \) is the galaxy inclination from face-on. This parameter \( W_{m}^{e} \) that approximates twice the maximum rotation velocity of a galaxy is the new linewidth parameter to be used in the correlation with luminosities, replacing the parameter \( W_{h}^{e} \) introduced by Tully & Fouqué (1985).

All the \( HI \) profiles used in the current analysis can be seen at the Web site http://edd.ifa.hawaii.edu by selecting the catalog “All Digital \( HI \),” then searching for the desired galaxy in that catalog and clicking on the name in the second column.

2.2. I-band Photometry

Photometry continues to accumulate, with the products by the Cornell group of particular note (Masters et al. 2006). Our recent own contribution was reported by Courtois et al. (2011a) where attention is given to ensure that the photometry in an approximation to the Cousins I band is consistent between authors.

Luminosities must be corrected for extinction internal to the target galaxies and our own Galaxy and for the displacement of flux due to Doppler shift. Extinction internal to the targets is usually the greatest concern. We follow the prescription given by Tully et al. (1998) who found that internal extinction has a pronounced luminosity dependence that can be described in terms of the rotation parameter. The inclination-dependent internal extinction at the I band is described by the expression

\[
A_{I}^i = \gamma_I \log(a/b) \quad \text{where} \quad a/b = \text{the major to minor axis ratio}, \tag{3}
\]

Arguments can be made for a more complex dependence of \( q_0 \), but we justify in Tully & Pierce (2000) our simplified choice.

Galactic extinction is important at low latitudes. We follow Schlegel et al. (1998), using the correction term \( A_{I}^i = R_{II} \) \((B-V) \) with differential reddening \( E(B-V) \) determined from 100\( \mu \)m cirrus maps and \( R_{II} = 1.77 \). The third adjustment, the \( k \)-correction, is very minor for the small redshifts we encounter. Chilingarian et al. (2010) recommend a correction which is more than adequate, \( A_{I}^i = 0.302z + 8.768z^2 - 68.680z^3 + 181.904z^4 \).

A fully corrected magnitude is

\[
I_{T}^{b,i,k} = I_T - A_{I}^i - A_{II}^i - A_{I}^k. \tag{4}
\]

3. NULLING BIAS

Our concern in this discussion is with one of two distinct “Malmquist biases” (Malmquist 1920, 1922, 1924). Confusion has arisen with Malmquist bias terminology so, to be clear, we are not at this point considering the bias that results from the volume sampling effect: either the first-order effect with a “homogeneous” distribution where a galaxy with a given measured distance is more likely to be more distant and scattered inward by error than nearer and scattered outward (Lynden-Bell et al. 1988) or the second-order effect with an “inhomogeneous” distribution where errors scatter measures out of higher into lower density regions (Strauss & Willick 1995). With the volume sampling Malmquist biases, individual distance measures may statistically scatter symmetrically about correct distances, yet a map of peculiar velocities might be biased, for example in the case of the homogeneous distribution case, due to the preponderance of inward over outward scattered distance measures since a more distant shell statistically contains more galaxies than a nearer shell of the same thickness. This potential bias can be minimized but the matter is better considered in the context of a velocity field analysis (Shaya et al. 1995).

The Malmquist effect that concerns us here is the one induced by a magnitude cutoff that can bias individual distance measures.\(^4\) Considering two galaxies with the same linewidth and at the same distance, the fainter one may be lost from

\(^4\) Strauss & Willick (1995) call this a selection effect rather than a Malmquist effect.
the sample while the brighter one is retained (Teerikorpi 1984; Sandage 1994; Theureau et al. 2007). Intuitively it will be expected that if galaxies intrinsically brighter than the mean tend to be selected, but are attributed the mean intrinsic luminosity, then galaxies will tend to be placed too close. This is the Malmquist bias. The amplitude of the bias depends on the slope attributed to the correlation. Intuition can be compromised; the bias can actually be reversed in sign by selecting a very steep slope because galaxies will tend to lie below the posited relation at the bright, high linewidth end. It follows that there is a slope that neutralizes the bias. This slope is given by a fit to the luminosity–linewidth correlation that assumes errors are entirely in linewidths, the “inverse TF relation” (Schechter 1980; Tully 1988; Tully & Pierce 2000).

A critical step in what follows is the construction of a template that gives the proper slope for bias-free distance measures. The template might be constructed from a cluster sample where all the galaxies are at the same distance and all appropriate galaxies are included down to a defined faint level. With a least-squares fit assuming errors are in linewidth, galaxies in each magnitude interval will scatter symmetrically about the fit. If this template relation is used to determine the distance to a galaxy in the field, the linewidth of that target galaxy will be drawn from the same symmetric distribution about the mean, as likely to be on one side of the relation in linewidth at a given magnitude as on the other. The distance measure will be unbiased.

This procedure involves several assumptions. It is assumed that the luminosity–linewidth correlation obeys a power law and that it is universal at the current epoch. It assumes that the scatter, which is both intrinsic and observational, is similar with both the template and the field targets. The procedure requires that the sample not be restricted in the linewidth measurements because any restrictions would carry the bias over to the orthogonal axis. The potential for bias depends on the luminosity function of normal gas-rich galaxies since if there are increasing numbers at fainter intervals then errors scatter more galaxies upward in luminosity than downward. Moreover, sample selections have not been made with strict $I$-band limits; rather, historically selections have been made from catalogs such as the Catalogue of Galaxies and Clusters of Galaxies (Zwicky & Kowal 1968) or the Uppsala General Catalogue (Nilson 1973) of the northern sky or the ESO/Uppsala Atlas (Lauberts 1982) of the southern sky. In these cases, selections are by photographic magnitude or diameter and transformations to the $I$ band involve color or surface brightness dependencies. Willick (1994) conducted a particularly thorough analysis of biases. He is a bit misleading in the abstract of that paper with the following statement:

“The use of the inverse method has been seen by some workers as a panacea for bias effects. A goal of this series is to show that in general the inverse method exhibits biases analogous to, though different in detail from, those exhibited by the forward relation.”

Willick goes on to show that while there can be bias with the inverse relation it is much reduced over the forward relation. In a concrete example (Willick et al. 1995) the bias correction is reduced by a factor of six from the forward relation, reducing the bias from a significant concern to a marginal effect. Masters et al. (2006), and before that Giovanelli et al. (1997a), have discussed the bias in the case of a bivariate formulation of the luminosity–linewidth relation where the bias is intermediate in amplitude. We will describe tests with simulations to estimate the level of bias pertinent to our procedures.

Preliminary to that we review properties of our sample. (1) Galaxies judged to be more face-on than 45° are excluded. Tests have not shown there to be any inclination dependencies in distance measures for samples restricted to this limit. Figure 1 shows that with our cumulative sample there are no systematics as a function of inclination in deviations from the mean relationship that is ultimately derived. There is not even any increase in scatter either toward 45° where linewidth projection uncertainties are greatest or toward 90° where absorption corrections are greatest. (2) Galaxies earlier in type than Sa are excluded. If S0 galaxies are accepted there is a substantial increase in scatter. Sa galaxies are on the cusp; sometimes they scatter badly. Exclusion on the basis of morphology introduces a clear basis for exclusion. (3) Galaxies are excluded if they are pathological, show pronounced evidence of tidal interactions, or have confused H I profiles. We tend to be inclusive if distortions are minor but contributions to the H I flux from multiple sources are a clear basis for exclusion. (4) Galaxies cannot be included if their H I profiles have inadequate signal to noise. The threshold requirement was discussed in Section 2.1. This restriction can be serious if it affects preferential parts of the correlation, for example, large linewidth systems where the flux per channel is reduced. We have addressed this issue by using long integrations to try to assure adequate coverage of calibrators. Galaxies too deficient to be reasonably detected are usually typical S0–Sa and are subject to elimination on the basis of morphology. It is to be noted that we do not impose a lower limit on linewidths nor do we reject based on line shape (e.g., single versus double peaked).
3.1. Bias in Simulations

While Malmquist selection biases are expected to be small using the inverse correlation Willick (1994) warns that they are not zero and the effect is systematic. We have run simulations to evaluate the amplitude of the problem. It was first established that the combined Virgo–Fornax–Ursa Major sample entailing 75 galaxies above an absolute magnitude limit \( M_f = -17.5 \) is described by a luminosity function (Schechter 1976) with bright end exponential cutoff parameter \( M^{*} = -23.0 \) and faint end power-law slope parameter \( \alpha = -1.0 \). A simulated luminosity–linewidth correlation was created by randomly drawing luminosities in accordance with the observed Virgo–Fornax–Ursa Major luminosity function and associating linewidths with a prescription that gave the desired correlation. Scatter to the relation was introduced by randomly drawing luminosities in accordance with the observed luminosity function, particularly the bright end attenuation fewer points are available to scatter down than up. Averaged over the ensemble to a specified magnitude limit, the result is an excess of points above the fiducial relation that is very small if the limit is faint but becomes increasingly important as the limit is moved brightward. The situation is aggravated if the faint limit cut is not at a constant magnitude but, rather, slopes upward with increasing linewidth as anticipated if selection is made in a blue band or diameter. Such selection favors inclusion of points above the fiducial relation over points below the fiducial relation. The slanting lines in Figure 3 illustrate limits at fixed \( B \) magnitudes with typical \( B–I \) colors for spiral galaxies (Tully et al. 1998). The amplitude of the bias in the simulated sample is shown in Figure 4 normalized to zero for the nearest three clusters (Virgo, Fornax, and Ursa Major) which are anchored by the zero-point calibration. The bias with flat magnitude limits is shown by the black open triangles and the bias with slanting color terms is shown by the red filled circles. It is seen that in the latter case the bias is only mildly increased. The solid curve approximates the "basket of clusters" approach taken by the Cornell group.

Differentials in magnitude with respect to the thick solid line in Figure 3 (the inverse luminosity–linewidth relation) correspond to differentials in measured “distance moduli,” with points above the line given distances farther than the mean and points below the line given distance farther than the mean. Bias arises from two effects. The more important one is generated by the form of the luminosity function, particularly the bright end attenuation. If the luminosity function invokes equal numbers per magnitude interval (our case at the faint end) then scatter upward and downward would be statistically equal and there would be no bias with a magnitude constant cut. However due to the bright end attenuation fewer points are available to scatter down than up. Averaged over the ensemble to a specified magnitude limit, the result is an excess of points above the fiducial relation that is very small if the limit is faint but becomes increasingly important as the limit is moved brightward. The situation is aggravated if the faint limit cut is not at a constant magnitude but, rather, slopes upward with increasing linewidth as anticipated if selection is made in a blue band or diameter. Such selection favors inclusion of points above the fiducial relation over points below the fiducial relation. The slanting lines in Figure 3 illustrate limits at fixed \( B \) magnitudes with typical \( B–I \) colors for spiral galaxies (Tully et al. 1998). The amplitude of the bias in the simulated sample is shown in Figure 4 normalized to zero for the nearest three clusters (Virgo, Fornax, and Ursa Major) which are anchored by the zero-point calibration. The bias with flat magnitude limits is shown by the black open triangles and the bias with slanting color terms is shown by the red filled circles. It is seen that in the latter case the bias is only mildly increased. The solid curve approximates the bias in this latter case. It obeys the equation \( b = 0.005(\mu - 31)^2 \) where \( b \) is the bias in distance modulus and \( \mu - 31 \) is the distance modulus normalized so \( b = 0 \) at moduli less than 31 (where sample magnitude limits are fainter than the useful range of the luminosity–linewidth correlation). The bias looks impressive in Figure 4 but it has a small effect on distance measures, reaching 3.5% in the most extreme case (A400). Cumulatively, the effect on the distances to the 13 calibrator clusters is 2%.

4. BUILDING A TEMPLATE

Our creation of a template from cluster samples is similar to the “basket of clusters” approach taken by the Cornell group.
### Table 1

Properties of the Cluster Fits

| Cluster | V\(_{\text{CMB}}\) | No. | Slope | eSI | ZP | rms | b | DM | eDM | Dist | eD | V/D | eH |
|---------|----------------|-----|-------|-----|----|-----|---|----|-----|------|----|-----|----|
| Virgo   | 1410           | 26  | −8.83 | 0.52 | 9.62 | 0.44 | 0.00 | 31.01 | 0.11 | 15.9 | 0.8 | 88.7 | 5.5 |
| Fornax  | 1286           | 15  | −8.57 | 0.56 | 9.80 | 0.41 | 0.00 | 31.19 | 0.12 | 17.3 | 1.0 | 74.3 | 5.2 |
| U Ma    | 1101           | 34  | −8.51 | 0.42 | 9.81 | 0.49 | 0.00 | 31.20 | 0.10 | 17.4 | 0.9 | 63.3 | 4.4 |
| Antlia  | 3119           | 14  | −9.83 | 1.03 | 11.42 | 0.30 | 0.04 | 32.85 | 0.10 | 37.2 | 1.7 | 83.8 | 4.2 |
| Cen50   | 3679           | 11  | −10.66 | 1.53 | 11.51 | 0.52 | 0.01 | 32.91 | 0.17 | 38.2 | 3.1 | 96.3 | 8.0 |
| Pegasus | 3518           | 17  | −7.56 | 0.76 | 11.89 | 0.42 | 0.00 | 33.18 | 0.12 | 43.4 | 2.5 | 80.9 | 4.8 |
| Hydra   | 4121           | 19  | −8.57 | 0.94 | 12.42 | 0.54 | 0.03 | 33.84 | 0.14 | 58.6 | 3.8 | 70.3 | 4.8 |
| Pisces  | 4779           | 58  | −9.45 | 0.56 | 12.62 | 0.40 | 0.01 | 34.02 | 0.08 | 63.8 | 2.4 | 75.0 | 3.0 |
| Cancer  | 4940           | 11  | −9.73 | 0.74 | 12.65 | 0.26 | 0.02 | 34.06 | 0.10 | 64.9 | 3.0 | 76.1 | 3.7 |
| Coma    | 7194           | 23  | −6.96 | 0.56 | 13.33 | 0.39 | 0.05 | 34.77 | 0.10 | 90.0 | 4.3 | 79.9 | 4.1 |
| A400    | 7108           | 7   | −8.25 | 2.14 | 13.40 | 0.24 | 0.07 | 34.86 | 0.11 | 93.8 | 4.8 | 75.8 | 4.2 |
| A1367   | 6923           | 19  | −9.26 | 1.03 | 13.42 | 0.39 | 0.05 | 34.86 | 0.11 | 93.8 | 4.7 | 73.8 | 3.9 |
| A2634   | 9063           | 13  | −8.86 | 1.00 | 13.98 | 0.39 | 0.04 | 35.41 | 0.13 | 120.8 | 7.1 | 75.0 | 4.6 |

**Notes.** Column information: (1) name; (2) velocity in CMB frame (km s\(^{-1}\)); (3) sample size; (4) slope determined for individual cluster; (5) slope uncertainty (68%); (6) zero point for individual cluster assuming universal slope (mag); (7) rms scatter in magnitude for individual cluster; (8) bias correction (mag); (9) distance modulus determined for individual cluster (mag); (10) uncertainty in cluster distance modulus (mag); (11) distance determined for cluster (Mpc); (12) uncertainty in cluster distance (Mpc); (13) “Hubble parameter” (velocity/distance) for individual cluster (km s\(^{-1}\) Mpc\(^{-1}\)); (14) uncertainty in Hubble parameter for individual cluster (km s\(^{-1}\) Mpc\(^{-1}\)).

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**Figure 4.** Bias as a function of cutoff magnitude. Open triangles: flat magnitude cutoff. Filled circles and solid curve: slanted magnitude cutoff at \(I\) band. Error bars are determined by repetitions varying the random number generator seed. Cutoffs for the 13 clusters are indicated by the abbreviated names above the bottom axis. (A color version of this figure is available in the online journal.)

(Giovanelli et al. 1997b; Masters et al. 2006; Springob et al. 2007). However there are differences. The Cornell group derive a slope from a bivariate fit to their template sample rather than an “inverse” fit with errors solely in linewidths. Their procedure requires a specification of the nature of scatter occurring along two axes, which is beyond our more relaxed assumption that scatter, whatever the source and the error partition between the axes, is similar for template and targets. We use fewer clusters but have more candidates per cluster.\(^5\) We need a significant number of galaxies per cluster to meaningfully test the universality of the luminosity–linewidth correlation and then to fit each contributing cluster to the template. With our 13 clusters, the median number of galaxies in our sample per cluster is 17, the mean is 20, and the maximum is 58. Finally, we do not provide a description of the correlation with variations that depend on type (Masters et al. 2006; Springob et al. 2007) or surface brightness (Theureau 1998). We view these variations as only marginally significant in the inverse correlations and they introduce complexity and subjectivity that may vary with distance.

The first step in the construction of the template involves developing inverse fits (errors in linewidths) to each of the 13 clusters separately. Results are displayed in Figures 5, and 6(a) and 6(b).

Here, the dotted lines illustrate the individual fits and the solid lines give the common slope that is ultimately derived; the latter fit to the individual clusters with only the zero point as a free parameter. Descriptors of the various fits are collected in Table 1. Clusters at successively greater distances have sample cutoffs at successively brighter intrinsic luminosities. However, on the assumption that each sample is being drawn from the same universal relationship, the slope of the inverse relation is the same (though less stable if sampled over a shorter range). By contrast, given the same scatter, the slope of a direct or bivariate fit becomes shallower as the sampling range diminishes! The run of the slopes determined for individual clusters as a function of distance is shown in Figure 7. No dependence with distance is seen; there is no evidence here of bias. The slopes for individual clusters do not differ significantly from the universal slope with the marginal exception of one case (Coma; see the discussion in the Appendix).

The nearest three clusters—Virgo, Fornax, and Ursa Major—are at similar distances and are sampled over a similar range in magnitudes. The search for a universal relation begins by establishing the best common least-squares fit slope and relative zero-point offsets that accommodate the three nearby clusters. The offsets were taken with respect to the Virgo Cluster and the fitting process quickly converged.

The remaining 10 clusters separate into three distance groups, Antlia, Centaurus, and Pegasus are \(\sim 2\) mag more distant than...
Virgo; Hydra, Pisces,\(^6\) and Cancer are \(\sim 3\) mag more distant; Coma, A1367, A400, and A2634 are \(\sim 4\) mag more distant. As a procedural matter, the template was successively augmented with the addition of each of these three groups from the nearer to the farther. Optimal slopes and zero-point offsets were determined at each step. Convergence was always rapid. The result is a definition of the universal slope and relative zero-point offsets representing the distance differences of each cluster with respect to the Virgo Cluster.

Interestingly, the scatters tend to decrease for the more distant clusters. One reason can be that scatter increases toward lower luminosities can be reduced with a recipe that accounts for the increasing importance of interstellar gas to the inventory of baryonic matter. Another reason can be that the nearby clusters are being resolved; the assumption that the targets are at a common distance is breaking down. Some attention to this matter is given in the Appendix for individual clusters.

The cumulative plot with clusters shifted to optimally fit the relationship at the Virgo distance is shown in Figure 8. This “template” of the new \(I\) band–H \(\beta\) linewidth correlation is built with 267 galaxies in 13 clusters extending in the range from 1000 km s\(^{-1}\) to 10,000 km s\(^{-1}\).

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\(^6\) The structure in Pisces is a filament rather than a cluster. The filament lies very close to the plane of the sky with little or no variation in distance along its length even though it extends across 20 Mpc. See the discussion in the Appendix.

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| PGC | Name    | \(\log W_{mx}\) | Inc | \(W_{mx}\) | \(W_{mx}\) | \(\log W_{mx}\) | DM | \(M_I\) |
|-----|---------|-----------------|-----|-----------|-----------|-----------------|----|--------|
| NGC 0055 | 6.88 | 86 | 166 | 166 | 0.222 | 26.62 | -19.74 |
| NGC 0224 | 1.34 | 78 | 517 | 528 | 0.372 | 24.48 | -23.14 |
| NGC 0247 | 7.79 | 76 | 190 | 196 | 0.292 | 27.84 | -20.05 |
| NGC 0253 | 5.07 | 81 | 410 | 415 | 0.261 | 27.83 | -22.76 |
| NGC 0300 | 7.28 | 46 | 140 | 195 | 0.259 | 26.59 | -19.31 |
| NGC 0598 | 4.74 | 55 | 177 | 217 | 0.236 | 24.82 | -20.08 |
| NGC 0925 | 8.96 | 57 | 194 | 231 | 0.364 | 29.81 | -20.85 |
| NGC 1365 | 8.09 | 54 | 371 | 459 | 0.662 | 31.27 | -23.18 |
| NGC 1425 | 9.50 | 65 | 354 | 391 | 0.592 | 31.70 | -22.20 |
| NGC 2090 | 9.33 | 67 | 277 | 301 | 0.478 | 30.35 | -21.02 |
| NGC 2366 | 11.03 | 74 | 90 | 94 | 1.972 | 27.57 | -16.54* |
| NGC 2403 | 7.11 | 60 | 226 | 261 | 0.417 | 27.50 | -20.39 |
| NGC 2541 | 10.76 | 63 | 188 | 211 | 0.325 | 30.25 | -19.49 |
| NGC 2841 | 7.53 | 66 | 592 | 650 | 0.813 | 30.74 | -23.81 |
| NGC 2976 | 8.98 | 60 | 129 | 149 | 0.173 | 27.77 | -18.79 |
| NGC 3021 | 10.92 | 57 | 254 | 303 | 0.481 | 32.27 | -23.15 |
| NGC 3031 | 5.20 | 59 | 417 | 485 | 0.686 | 27.81 | -22.61 |
| NGC 3109 | 9.15 | 90 | 110 | 110 | 0.241 | 25.62 | -16.47* |
| NGC 3198 | 9.17 | 70 | 296 | 315 | 0.249 | 30.70 | -21.53 |
| NGC 3201 | 10.12 | 69 | 106 | 113 | 0.204 | 25.76 | -17.84 |
| NGC 3351 | 8.33 | 47 | 262 | 359 | 0.556 | 30.00 | -21.67 |
| NGC 3370 | 10.85 | 58 | 264 | 312 | 0.494 | 31.13 | -21.28 |
| NGC 3368 | 8.01 | 66 | 266 | 292 | 0.465 | 29.08 | -21.07 |
| NGC 3621 | 7.39 | 60 | 333 | 385 | 0.585 | 29.59 | -22.20 |
| NGC 4244 | 8.92 | 90 | 192 | 192 | 0.283 | 28.16 | -19.24 |
| NGC 4258 | 6.84 | 69 | 415 | 444 | 0.647 | 29.41 | -22.57 |
| NGC 4414 | 8.73 | 65 | 378 | 463 | 0.666 | 31.24 | -22.51 |
| NGC 4535 | 8.95 | 45 | 265 | 374 | 0.573 | 30.09 | -22.04 |
| NGC 4536 | 9.03 | 71 | 322 | 341 | 0.533 | 30.91 | -21.88 |
| NGC 4605 | 9.19 | 70 | 154 | 165 | 0.229 | 28.71 | -19.52 |
| NGC 4603 | 9.76 | 52 | 353 | 450 | 0.653 | 32.60 | -22.84 |
| NGC 4639 | 10.18 | 55 | 274 | 336 | 0.526 | 31.67 | -21.49 |
| NGC 4725 | 7.84 | 58 | 397 | 470 | 0.585 | 29.59 | -22.20 |
| NGC 4945 | 6.30 | 86 | 358 | 359 | 0.555 | 27.63 | -21.33 |
| NGC 5584 | 10.62 | 44 | 186 | 267 | 0.426 | 31.72 | -21.10 |
| NGC 7331 | 7.52 | 66 | 501 | 547 | 0.273 | 30.72 | -23.20 |
| NGC 7793 | 8.25 | 53 | 162 | 202 | 0.236 | 27.79 | -19.54 |

Notes. Column information: (1) Principal Galaxy Catalog ID; (2) name; (3) apparent \(I\)-band magnitude corrected for Galactic and internal reddening and redshift; (4) inclination from face-on; (5) linewidth at 50% of mean flux with adjustments to statistically represent twice maximum projected rotation velocity (km s\(^{-1}\)); (6) linewidth parameter de-projected to edge-on orientation (km s\(^{-1}\)); (7) logarithm of de-projected linewidth parameter; (8) distance modulus from independent (Cepheid or TRGB) distance measurement; (9) Absolute \(I\)-band magnitude at the independently determined distance. The two alerts signaled by * identify galaxies fainter than the range encompassed by the template slope calibration and not used in the zero-point calibration.

5. INTRINSIC ZERO POINT

There are increasing numbers of relatively nearby galaxies appropriate for the luminosity–linewidth methodology with independent distance measures of reasonable accuracy. We accept the zero point established by the Hubble Space Telescope distance scale project (Freedman et al. 2001) and the distances to galaxies from Cepheid period–luminosity measures consistent with that scale. We also accept measures from the tip of the red giant branch method that have been shown to be on a consistent scale (Rizzi et al. 2007). The maser distance to NGC 4258 is also taken into account (Herrnstein et al. 1999). Information about the zero-point calibration sample is collected in Table 2.
Figure 6. (a) $I$-band luminosity–linewidth correlations for 15 galaxies in Fornax, 34 galaxies in Ursa Major, 14 galaxies in Antlia, 11 galaxies in Centaurus, 17 galaxies in Pegasus, and 19 galaxies in Hydra. Solid lines are the universal template fits and dotted lines are fits to the individual clusters. In the case of the Fornax Cluster, galaxies superimposed on the central core are identified with larger symbols, galaxies in the periphery are identified by smaller symbols, and one rejected galaxy is identified by an open symbol. See the Appendix for discussions of individual clusters. (b) $I$-band luminosity–linewidth correlations for 58 galaxies in Pisces, 11 galaxies in Cancer, 23 galaxies in Coma, 7 galaxies in A400, 19 galaxies in A1367, and 13 galaxies in A2634. Solid lines are the universal template fits and dotted lines are fits to the individual clusters. In the case of the Pisces filament galaxies lying at SGB < 5 are identified by filled symbols and galaxies north of this limit are identified by open symbols. See the Appendix for discussions concerning Pisces and the other clusters.

The luminosity–linewidth relation found with these galaxies with independent distances is shown in Figure 9 now on an intrinsic luminosity scale. These galaxies do not represent a magnitude limited sample so a slope fit to these data would be inappropriate. The fit illustrated by the solid line has the slope defined by the 13 cluster templates and a zero point established from a least-squares fit to the 36 calibrators that lie within the magnitude range of the template. The sample of zero-point calibrators is consistent with being drawn from the universal correlation.

The magnitude scale relations between the fits in Figures 8 and 9 give a distance modulus for the Virgo Cluster and, from the offsets built into Figure 8, give distance moduli for the other clusters. The combined cluster and zero-point calibrator samples are shown together in Figure 10. The associated distances are recorded in Table 1. If our fully corrected luminosity and H$\text{I}$ profile parameters are employed then the distance modulus of a galaxy $\mu = I_{b,i,k} - M_{b,i,k}^h$ can be calculated from the relation between linewidth and absolute magnitude

$$M_{b,i,k}^h = -21.39 - 8.81(\log W_{\text{mx}}^i - 2.5),$$

where $1\sigma$ uncertainties are $\pm0.07$ in the zero point and $\pm0.16$ in the slope. The rms scatter about the mean relation for the ensemble of 267 template galaxies is $\pm0.41$ mag corresponding to a scatter in distance of 21%. Some of this scatter must be contributed by the finite depth of the clusters. The rms scatter about the mean for the 36 zero-point calibrators with Cepheid or TRGB distances is $\pm0.36$, not substantially less.

Hubble parameters (velocity/distance) for the 13 clusters are displayed as a function of velocity in the cosmic microwave background frame in Figure 11. The Hubble parameter gyrates wildly within 50 Mpc ($V_{\text{CMB}} < 4000$ km s$^{-1}$), the region of the Local Supercluster and the Great Attractor, but shows little variation for the seven most distant clusters. A fit to those outer seven clusters gives the result $H_0 = 75.1 \pm 2.7$ km s$^{-1}$ Mpc$^{-1}$ with a standard deviation of $\pm1.0$ km s$^{-1}$ Mpc$^{-1}$.

6. LITERATURE COMPARISONS

We first make a comparison with our earlier calibrations using similar procedures. The new calibration uses digital rather than analog H$\text{I}$ information with a different definition of linewidth
and enlarged slope and zero-point samples but distances for 12 clusters in common with the Tully & Pierce (2000) study are overall only slightly increased (new cluster distances are larger by 1.4%) although the most distant clusters are set back 5%, mostly due to the bias correction that is now introduced. Tully & Pierce found $H_0 = 77 \text{ km s}^{-1} \text{ Mpc}^{-1}$. Studies with the same methodology a decade earlier (Shaya et al. 1992) had suggested $H_0 = 88 \text{ km s}^{-1} \text{ Mpc}^{-1}$ but Tully & Pierce pointed out that most of the reduction in $H_0$ by 2000 resulted from an improved zero point with the availability of Cepheid distances from the HST distance scale key project.

Now giving attention to studies from independent researchers, we find that there are sufficient overlaps for meaningful comparisons with two existing samples. The first one to consider is a separate analysis with the same methodology. We give attention to the Cornell group results for clusters presented by Masters et al. (2006). Before making the comparison we undid a correction made by Masters et al. that appears to us to be erroneous. They correctly point out that the true distance of a cluster is statistically greater than the value implied by the average of the measured moduli but they overestimate the effect by an order of magnitude. They give “corrections” for the effect that range from 5% for the nearest clusters to 0.5% for the most distant. From simulations we determine corrections of 0.5% for the nearest three clusters (which we incorporate) and negligible corrections for the rest. As a practical matter, only Fornax and

![Figure 6](Continued)

**Table 3**

| Cluster | This Paper | TP00  | SFI++ | ENEARc | SMAC  |
|---------|-----------|-------|-------|--------|-------|
| Virgo   | 15.9 ± 0.8 | ...   | ...   | 17.1 ± 0.8 | 15.4 ± 0.9 |
| Fornax  | 17.3 ± 1.0 | 17.8  | 19.6 ± 1.3 | 17.5 ± 1.1 | ...  |
| U Ma    | 17.4 ± 0.9 | 18.6  | 17.9 ± 1.2 | ...   | ...  |
| Antlia  | 37 ± 2   | 36    | 40 ± 2  | 40 ± 2  | 44 ± 2 |
| Cen30   | 38 ± 3   | 40    | 40 ± 2  | 40 ± 2  | 44 ± 2 |
| Pegasas | 43 ± 3   | 46    | 51 ± 3  | 52 ± 6  | ...  |
| Hydra   | 59 ± 4   | 58    | 58 ± 3  | 59 ± 3  | 56 ± 3 |
| Pisces  | 64 ± 2   | 60    | 64 ± 4  | 66 ± 4  | 67 ± 3 |
| Cancer  | 65 ± 3   | 62    | 65 ± 4  | ...    | ...  |
| Coma    | 90 ± 4   | 86    | 91 ± 5  | 109 ± 5 | 105 ± 4 |
| A400    | 94 ± 5   | 92    | 91 ± 5  | ...    | ...  |
| A1367   | 94 ± 5   | 86    | 90 ± 5  | 103 ± 10 | 92 ± 7 |
| A2634   | 121 ± 7  | 111   | 116 ± 7 | 162 ± 12 | 134 ± 6 |

**Notes.** Distances and errors in Mpc. Literature sources: TP00 (Tully & Pierce 2000); SFI++ (Masters et al. 2006); ENEARc (Bernardi et al. 2002); SMAC (Hudson et al. 2001).

Ursa Major are affected in the present comparison since Masters et al. did not consider the Virgo Cluster.

Our separate results are given in Table 3 for the 12 clusters in common (i.e., excluding Virgo). There is a good agreement. It is to be recognized that the results are hardly independent. Most
Figure 7. Correlation slope determined for individual clusters as a function of distance. The solid line shows the slope of $-8.81$ given by the fit to the ensemble of 13 clusters.

Figure 8. Cumulative plot superimposing data from 13 clusters with zero-point offsets relative to the Virgo Cluster. The solid line is least-squares fit to the ensemble with errors in linewidths. (A color version of this figure is available in the online journal.)

Figure 9. Zero-point calibration based on 36 galaxies with distances independently established with either Cepheid period–luminosity or tip of the red giant branch measures. The solid line is the least-squares fit with the slope fixed to the value established by the 13 cluster templates. (A color version of this figure is available in the online journal.)

Figure 10. Zero-point calibrator and 13 cluster template samples combined. The absolute magnitude scale for the cluster sample is set by the fit to the zero-point calibrators. (A color version of this figure is available in the online journal.)

(not all) of both the raw H\textsc{i} profile and I-band photometry data are used in common. Both studies avail of Cepheid distances from the HST key project to set zero points. Looking in detail, the worst individual match is in the case of the Pegasus Cluster where the disagreement is at the level of 2\sigma. There is the disturbing systematic of poor agreement with the clusters nearer than 4000 km s$^{-1}$. Masters et al. place these five clusters more distant by 10\% with a statistical significance of 4\sigma. On the other hand there is agreement with the seven more distant clusters at the level of 2\% in the mean and with a per cluster scatter of only 2\%.

The disagreement with the nearer clusters remains to be clarified. If attention is restricted to clusters beyond 4000 km s$^{-1}$, it is seen from Figure 11 that we derive $H_0 = 75$ km s$^{-1}$ Mpc$^{-1}$ from this limited sample. Masters et al. determined a value of $H_0 = 74$ km s$^{-1}$ Mpc$^{-1}$ from a more extensive sample beyond 4000 km s$^{-1}$.
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Figure 11. Run of the Hubble parameter (velocity in the CMB frame/distance) as a function of distance. The fit to cluster points at distances greater than 50 Mpc ($V_{\text{CMB}} > 4000 \text{ km s}^{-1}$) corresponds to $H_0 = 75.1 \text{ km s}^{-1} \text{ Mpc}^{-1}$.

The second comparison to be made is with fundamental plane measurements where the material is entirely independent. We compare two distinct fundamental plane samples: one with the acronym ENEARc (Bernardi et al. 2002) and the other called SMAC (Hudson et al. 2001). We mention in passing that we have re-analyzed both of these data sets using “inverse” relationships analogous to the “inverse” relation between rotation and luminosity in spirals and we find distances in excellent agreement with those found by the authors of the ENEARc and SMAC studies; in other words, the inverse fits effectively nullify bias without corrections. However, for the present comparisons we draw on the distance determinations given by the original authors.

The zero point that we accept for the fundamental plane measurements comes from the comparison between this method with the SMAC sample and the surface brightness fluctuation method (Blakeslee et al. 2002). Tiny corrections are made to the surface brightness fluctuation distances following Blakeslee et al. (2010). The zero point is extended to the ENEARc sample by a comparison of distances for 18 clusters in common with the ENEARc and SMAC studies.

Alternative distances for clusters in our program are reported in Table 3 and graphical comparisons are made in Figure 12. A systematic offset is seen. If we accept a slope of unity in the fit to measures as a function of distance then the offset is 9% in distance, fundamental plane measures larger, with 4σ significance and 10% scatter per individual cluster. There is a hint that the slope in the data of Figure 12 is slightly flatter than unity but the significance is only 2σ.

There are some issues that remain to be reconciled. With the surface brightness fluctuation zero point, the cumulative ENEARc and SMAC samples are consistent with $H_0 = 72 \text{ km s}^{-1} \text{ Mpc}^{-1}$. A renormalization of those samples to agree with our distances for nine of their clusters would imply $H_0 = 78 \text{ km s}^{-1} \text{ Mpc}^{-1}$. On the other hand, Tully et al. (2008) report agreement between surface brightness fluctuation and luminosity–linewidth distances in Cosmicflows-1.

Figure 12. Comparison of distance moduli from this paper with fundamental plane moduli. Filled symbols: ENEARc; open symbols: SMAC.

Conflicts will not be resolved in the present work. They will be given further attention with the integration of distances derived with these methods and several others during the compilation of Cosmicflows-2.

7. CONCLUSIONS

A re-calibration of the relationship between galaxy rotation rates and luminosities is necessitated by the initiation of a new way of measuring H I profile linewidths. Our purpose is to measure distances and in this case we advocate use of the “inverse” relationship that almost nulls the magnitude limit Malmquist (selection) bias. There is a residual correction that affects the measure of $H_0$ at the level of 2%. If the purpose were to try to understand the origins of the luminosity–rotation relationship it would be advisable to give attention to a description given by the bivariate fit. In this case and with our parameters, $L_I \propto W_3^{0.4 \pm 0.1}$.

There can be concern about whether the relationship is the same in different environments, i.e., whether there is a “universal” form at the present epoch. We have explored the situations in 13 different environments ranging from high-density collapsed regions dominated by early-type systems to extended low-density regions dominated by gas-rich systems (see the Appendix for details). The samples from all 13 environments are consistent with being drawn from a single universal distribution. Masters et al. (2006) have reached a similar conclusion. It is true that there are more aberrant cases in the collapsed cores of clusters. The harsh environments of clusters probably do have an effect. For our purposes there may be an ameliorating circumstance. The spiral galaxies seen in and around rich clusters may mostly be recent arrivals. Anyway, empirically there is no evidence contrary to the proposition that the calibration is representative.

The scatter in magnitude about the mean relationship is characteristically 0.4 mag which translates to 20% uncertainty in a distance estimate. As Giovanelli et al. (1997b) have pointed out, the scatter is less at high luminosities and greater at
low luminosities. Fractional uncertainties are largest for fainter galaxies with narrower linewidths and for more face-on galaxies requiring larger de-projection corrections. As Verheijen (2001) has demonstrated, the scatter can be reduced with sample pruning and resolved kinematic information. There are claims of type and surface brightness dependencies. These diminish toward the infrared and with the steeper "inverse" slope to the extent that the second parameter dependencies become marginal and undesirable to implement because they introduce small discontinuities and subjectivity that may be distance dependent. Sensitivity to distance diminishes with the steeper inverse slope but the offsetting benefits are diminished bias and enhanced simplicity.

The comparison with alternative distance measures, particularly fundamental plane measures, demonstrates overall agreement and small scatter but there are still unresolved zero-point issues at the 9% level. The full construction of Cosmicflows-2 will involve information from considerably more sources and hopefully the zero-point issues will be resolved or at least diminished. From the fits with our data alone and restricted to the seven clusters at $V_{\text{CMB}} > 4000$ km $s^{-1}$ we infer $H_0 = 75.1$ km $s^{-1}$ Mpc$^{-1}$. The formal standard deviation is a ridiculously small 1 km $s^{-1}$ Mpc$^{-1}$ but the sample is small, there are remaining zero-point uncertainties, and then, as hinted at with the large local deviations in Figure 11, there is the undisputed issue of velocity perturbations on large scales. There is still work to do.

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APPENDIX

CLUSTER SAMPLE DETAILS

Galaxy clusters are rarely simple structures. The following discussion summarizes issues arising with each of the 13 clusters.

Virgo Cluster. This cluster was not included in the catalog by Abell (1958) because of its proximity, but it comfortably qualifies as an Abell cluster of richness class zero. It is a good candidate for our study because it contains many spirals as well as early-type systems. Probably many of the spirals in the cluster are recent arrivals because galaxies are seen to be falling into the cluster along a filament known as the Virgo Southern Extension (Tully & Shaya 1984). Within the cluster, galaxies have observed velocities ranging between $-600$ and 2800 km $s^{-1}$. The systems with blueshifts are virtually certain to be cluster members (Sandage 1978) but the wide range in redshifts could conspire to conceal contaminants. Indeed, the Virgo W Cluster (de Vaucouleurs 1961) is centered slightly to the southwest of the Virgo Cluster in projection, contains galaxies with velocities 1700–2700 km $s^{-1}$, but lies at about twice the distance of the Virgo Cluster. Some galaxies associated with Virgo W can be expected to project onto the Virgo Cluster, including those in the Virgo M structure (Ftaclas et al. 1984). The Virgo W Group lies at an intermediate distance in the background. Surface brightness fluctuation observations (Blakeslee et al. 2009) confirm this picture. Our own most recent compilation of CosmicFlows-1 distances can be culled to map the structure in the region of the Virgo Cluster (Tully et al. 2008). Projection contaminants do exist but fortunately all the known problems are confined to the western and southwestern sectors involving $\sim 40\%$ of the area of the cluster. There are no documented contaminants in the central and eastern sectors (Trentham & Tully 2002) except for the dwarf GR8 that lies just outside the Local Group.

Figure 13 shows the distribution of galaxies at large around the Virgo Cluster and of the specific sample used in the cluster.
The circle at radius $6.8 = 2.0$ Mpc lies at what we infer to be the radius of second turnaround (Tully 2010) which is closely related to the virial radius. We only accept candidates that project onto the collapsed cluster and in the region free of known contaminants.

The correlation between luminosity and rotation rate was shown in Figure 5. One $4\sigma$ outlier is identified by the open symbol. This system, PGC42081=IC3583, is an irregular galaxy with a measured distance assuming the mean relation of only 7 Mpc, i.e., well to the foreground. Plausibly, given its heliocentric velocity of 1121 km s$^{-1}$, this galaxy lies near the foreground zero velocity surface, at the interface between cosmological expansion and cluster infall. This galaxy is excluded from the Virgo Cluster fit. From the other 26 candidates a modulus of $31.01 \pm 0.10 \ (15.9 \pm 0.8 \ Mpc)$ is determined. This distance to the Virgo Cluster is consistent with the distance of $16.5 \pm 1.1 \ Mpc$ favored by Blakeslee et al. (2009) reporting on the surface brightness fluctuation project with Hubble Space Telescope.

**Fornax Cluster.** In contrast to the Virgo Cluster, the smaller Fornax Cluster has few spiral galaxies in its core. It is necessary to accept candidates at somewhat larger distances to accumulate a large enough sample. In the top panel of Figure 14 one sees a wide view of the Fornax environment and in the bottom panel there is a zoom into the central region (rotated to supergalactic coordinates) and a display of the useful candidates.

The red and blue circles in the top panel of the figure illustrate (crudely) second and first turnaround surfaces around the major collapsed regions (halos) in the Fornax–Eridanus region. There is little correlation between velocity and distance across this region and first turnaround surfaces between adjacent halos are strongly overlapping. There is the implication that the entire region will ultimately collapse. See Brough et al. (2006) for a further discussion.

Several separate halos lie in close proximity to the Fornax Cluster core, taken to center on NGC 1399. The most important, and overlapping, is centered on NGC 1316. A third, abutting, is centered on NGC 1344. The sample of 43 early-type galaxies in the surface brightness fluctuation study by Blakeslee et al. (2009) spills from the NGC 1399 core into the NGC 1316 and NGC 1344 regions. All three regions are at the same distance to within measurement errors in that study. Less than half of our candidates lie within the dominant halo identified in Figure 14 but, for our purposes, the issue is not whether a candidate lies within the central halo but whether it lies close enough to the others in distance to be statistically representative. The luminosity–linewidth correlation was shown in Figure 6(a). The large symbols represent galaxies projected onto the central Fornax halo while the small symbols represent galaxies outside the core. No statistically significant difference is seen in either component from the fit to the ensemble. Within the measurement errors all the galaxies in the region are at the same distance, a result consistent with that found by Blakeslee et al.

One galaxy, PGC13794=NGC 1437B, with an excursion of $4\sigma$ is deleted from the fit. This galaxy has alternatively been classed Sa and I0 and has a strikingly asymmetric H$\alpha$ profile. The galaxy has probably experienced stripping.

The fit to the remainder of the candidates results in a modulus of $31.19 \pm 0.11 \ (17.3 \pm 0.9 \ Mpc)$. The differential distance modulus with respect to the Virgo Cluster is $0.18 \pm 0.13$, which is a $2\sigma$ deviation from the Blakeslee et al. (2009) differential modulus of $0.42 \pm 0.03$.

**Ursa Major Cluster.** Perhaps the association of galaxies in Ursa Major should not be called a cluster although it is substantial enough to only fail the Abell richness class zero definition by a couple of galaxies (Tully et al. 1996). However, with galaxies spread across a long axis of over 4 Mpc and a velocity dispersion of only 148 km s$^{-1}$ the structure involves
more than a single parent halo. Most of the galaxies in the region are gas rich spirals and irregulars with a couple of separated knots of early-type galaxies. Although contamination could be expected because the entity is in the plane of the Local Supercluster, problems are minimized by the limited velocity window \((700 < V_h + 300 \sin \ell \cos b < 1210 \text{ km s}^{-1})\) and there is no evidence of interlopers. For the present discussion, at issue is whether the galaxies in the structure are at similar distances. We find no differences in distances by location or velocity. If the structure has a line-of-sight depth comparable to the projected long axis dimension then a dispersion of \(\sigma_{\text{los}} = 0.17\) mag will contribute to the observed dispersion.

To date, the most ambitious analysis of the luminosity–linewidth correlation in a single cluster was a study with the Westerbork Synthesis Radio Telescope (WSRT; Verheijen & Sancisi 2001; Verheijen 2001). The sample in the present study is almost the same as Verheijen’s RC (rotation curve) sample. We add six systems that were not observed with WSRT but have single beam profiles (PGC’s 36875, 37038, 37832, 38951, 39344, 40537) and remove three that are considered confused or morphologically inappropriate (PGC’s 35711, 38375, 38643).

Verheijen (2001) confirmed the finding by Bernstein et al. (1994) with a Coma Cluster study that with judicious morphological and \(\text{H}1\) profile preselection (non-interacting, Sb to Sd, steep \(\text{H}1\) profile edges, smooth outer contours, no bar) the correlation between luminosity and linewidth is much tighter \((\sigma \sim 0.2–0.3)\) than we find with a larger, less restrictive sample. When Verheijen gave attention to his RC sample that approximates our own he found two factors in detailed velocity maps that correlate with dispersion. One of these is found in relatively luminous and earlier typed spirals where RCs are observed to peak and then drop to a lower velocity in the outer reaches. Verheijen found that if a linewidth measure based on a global profile is used (or alternatively, a measure of the maximum velocity), then luminous, early-type galaxies scatter to larger linewidths at a given luminosity, but if a linewidth measure indicative of the outer rotation that he calls \(V_{\text{flat}}\) is used, then offsets from the mean relation are removed. The other correlation with dispersion occurs at the opposite end of the relation, with relatively faint systems, where RCs are observed to still be rising at the outermost \(\text{H}1\) contours. These galaxies tend to lie to smaller linewidths at a given luminosity, suggesting that the gas is too restricted to sufficiently probe the halo potential. Both of these clarifications concerning the correlation scatter are edifying but cannot be usefully incorporated if only global profiles are available.

Several other conclusions by Verheijen (2001) are worth noting. He did not find any convincing second parameters in the near-infrared correlation although correlations at the \(B\) band were found in the sense that early, high surface brightness, red galaxies lie faintward of late, low surface brightness, blue galaxies at a given linewidth. The color dependence negates the offsets in the infrared. Verheijen also confirmed the improvement to the correlation found by McGaugh et al. (2000) if luminosity is replaced with a measure that sums the mass in stars and the mass in gas (the baryonic mass).

In summary of this discussion, the spatially resolved kinematic study by Verheijen (2001) clarifies several issues but these go beyond what is useful for our present purposes. We only have access to global profiles and we want a methodology that minimizes subjective restrictions based on morphology. The methodology should be as inclusive as possible and not have characteristics that might be interpreted differently as a function of distance.

The luminosity–linewidth correlation for the Ursa Major association is shown in Figure 6(a) and the distance modulus determined from 34 galaxies in that correlation is \(31.20 \pm 0.10\) \((17.4 \pm 0.9\) Mpc). By contrast, the distance modulus to seven early-type galaxies in Ursa Major from surface brightness fluctuation measurements (Tonry et al. 2001) is \(30.69 \pm 0.10\) \((13.7 \pm 0.7\) Mpc), a difference with 3.6\(\sigma\) significance from our value. Overall around the sky there is agreement between surface brightness fluctuation and luminosity–linewidth measures (Tully et al. 2008), but this significant difference in Ursa Major remains an abiding mystery.

Antlia and Hydra Clusters. These two clusters are treated together because, although they are at quite different distances, they lie close to each other on the sky and their velocity ranges overlap. Confusion is possible. The top panel of Figure 15 shows the distribution of galaxies in the neighborhood with systemic velocities indicated by colors and the collapsed cores of the two clusters shown by circles: Antlia to the lower left with smaller velocities and Hydra to the upper right with larger velocities. In the bottom panel of this figure the green triangles and red circles, respectively, locate the galaxies that constitute the Antlia and Hydra samples. In both cases, the samples spill outside the core regions, extremely so in the case of the Antlia Cluster. Both clusters are dominated by early-type systems in the collapsed cores. Two of the Antlia candidates lie in the direction of the Hydra Cluster and might be a particular concern, but both are more consistent in velocity and measured distance with membership in Antlia. The luminosity–linewidth diagram for these two clusters is seen in Figure 6(a). The scatter in the Antlia plot is particularly small, minimizing concerns about depth variations though the sample is scattered on the sky. By contrast the spatially more compact Hydra sample manifests the greatest correlation scatter of any of the clusters. Still, the slope derived from the Hydra Cluster alone is in excellent agreement with that of the 13 cluster ensemble.

The Antlia Cluster is determined to have a distance modulus of \(32.85 \pm 0.10\) \((37.2 \pm 1.7\) Mpc). This value is in good agreement with the average of three galaxies in Antlia with surface brightness fluctuation measurements (Tonry et al. 2001) of \(32.64 \pm 0.14\) \((33.7 \pm 2.4\) Mpc). The modulus of the Hydra Cluster is \(33.84 \pm 0.14\) \((59 \pm 4\) Mpc). This result is in poor agreement with the surface brightness fluctuation measure by Mieske et al. (2005) of \(33.07 \pm 0.07\) \((41.2 \pm 1.4\) Mpc), a 5\(\sigma\) excursion from our value.

Centaurus Cluster. Two distinct kinematic structures in the line of sight complicate the situation with this cluster. The complexity is described by Stein et al. (1997). In a histogram of velocities there is a narrow peak at 4750 km s\(^{-1}\) superposed on a broad distribution centered at 3400 km s\(^{-1}\). The spatial centroid of the higher velocity component is displaced on the sky from the centroid of the broad distribution. The two components have come to be referred to as the high velocity Cen45 and the low velocity Cen30 (Lucey et al. 1986). Alternatively, the two features could be at distinct distances in projection (Faber et al. 1989) or in the process of merging, and hence at similar distances (Lucey & Carter 1988).

The current effort is to calibrate a way to measure distances so we want to avoid controversy that will be resolved by measuring distances. Consequently we impose a restriction on velocities for this sample, \(V_h < 4000\) km s\(^{-1}\), that excludes any Cen45 contribution.
The luminosity–linewidth correlation found with the resultant sample is displayed in Figure 6(a). The scatter is uncharacteristically large. Figure 16 shows the sky projection of candidates. They lie within or very close to the cluster core defined by an estimate of the second turnaround collapse radius. There is the curiosity that the most deviant cases brighter than the mean relation ($\Delta \mu > 0.4$) lie on one side of the cluster (at more positive supergalactic latitudes) while the most deviant in the opposite sense ($\Delta \mu < -0.4$) lie on the other side. There might be a hint here of a depth effect, but the lower panel of Figure 16 provides no support. In this plot, scatter from the mean relation is interpreted as distance offsets which are plotted against systematic velocity but there is no suggestion of the S-wave of infall that would be anticipated. Nor is there a hint of the Hubble relation with distance. Our conclusion is to take the sample at face value, as representative of the Cen30 cluster with
unexplained enhanced scatter. The data support a distance modulus of 32.91 ± 0.16 (38 ± 3 Mpc). By comparison Mieske et al. (2005) found 33.28 ± 0.09 (45 ± 2 Mpc) from a surface brightness fluctuation study. The difference is 0.37 ± 0.18, roughly 2σ. Most perplexing, though, is that we find the Centaurus cluster to lie 0.93 ± 0.21 convincingly in front of the Hydra cluster while Mieske et al. claim that Centaurus is 0.21 ± 0.11 behind Hydra.

**Pisces filament.** If there is doubt that the Ursa Major region should be considered a cluster, it is certain that the region we will consider in the well-studied Perseus–Pisces Supercluster (Wegner et al. 1993) is not just a cluster. It can be seen from the distribution of the sample in Figure 17 that galaxies are being considered over a projected long axis extent of 20 Mpc. There are several knots dominated by early-type systems (and so not represented in our figure), most prominently a cluster around NGC 507 and the A262 cluster. The inferred second major axis of Cosmicflows-1 that the dispersion along a segment of the Pisces filament is small and implied unmeasurable depth (Tully & Pierce 2000). Hudson et al. (1997) acquired distances along a larger segment of the Perseus–Pisces chain using the fundamental plane methodology and, while they found variations in distance along the full length, they could not see any distance variations along the length that interests us.

In an initial fit, all 58 galaxies in the sample are considered. The slope fit to this sample alone is in good agreement with the 13 cluster “universal” slope. A fit constrained to the universal slope and with a zero point established by the local calibrators results in a distance modulus of 34.02 ± 0.06 (64 ± 2 Mpc). The rms scatter is ±0.43. It was noticed, though, that the most deviant points lie at the north end of the filament (in supergalactic coordinates). To test for variations along the filament we split the sample into three parts: (1) SGB > 5, (2) nearest NGC 507, and (3) nearest A262. The mean modulus, dispersion, and sample size for the three parts and for the ensemble are summarized in Table 4. The results are clear. There are no significant differences between any of the moduli. However, the scatter is much greater in the subsample at SGB > 5; rms scatter of ±0.53 in magnitude for 26 galaxies compared with ±0.34 for 32 galaxies at SGB < 5. The scatter in the southern subsample is amazingly low, leaving little place for depth effects. By contrast, the scatter in the northern subsample is large and an obvious explanation would be a contribution from distance variations. Nevertheless, the fit to the ensemble of 58 galaxies discussed in the previous paragraph is representative within certainties of all the subsamples and the rms scatter for the ensemble, averaged over the exceptional south and the spotty north, is about normal. The luminosity–linewidth relation is seen in Figure 6(b).

**Coma Cluster.** This cluster merits special attention. While the Ursa Major and Pisces regions are representative of moderate density environments dominated by gas-rich galaxies, Coma Cluster represents the high density extreme, a place dominated by gas-poor systems. Observations of the sample present compounded difficulties: the targets are faint in H i flux both because they are far away and because they are intrinsically H i deficient. For the clusters that have been discussed up to now H i detections are generally not a challenge. With the Coma sample longer integrations were sometimes required to obtain adequate spectra. With considerable effort, essentially all our original candidates are usefully detected.

As an extra motivation, Bernstein et al. (1994) have reported that the dispersion in the luminosity–linewidth relation is very small in Coma. Is the slope of the correlation consistent with that found in other clusters?

Our version of the relation is shown in Figure 6(b). Indeed, the dispersion is small (rms of ±0.27 mag) about a slope to this sample of −6.96 ± 0.56. The difference between the two slopes in the figure has a statistical significance of 3σ. It is seen in Figure 7 that all the other individual cluster slopes are within ∼1σ of the mean slope. In the case of Coma the error bar is small because the scatter around the shallow slope is small.

Figure 18 shows the locations of the sample in relation to the cluster. The sample candidates are not very concentrated. Only 6 of 23 lie within the region of collapse. The open symbols identify systems that deviate by more than 0.4 mag from the fit with the universal slope; squares to the bright side and triangles

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**Table 4**

| Sample    | Modulus  | rms     | No. |
|-----------|----------|---------|-----|
| SGB > 5   | 34.07 ± 0.10 | ±0.53  | 26  |
| NGC 507   | 33.92 ± 0.08 | ±0.31  | 15  |
| A 262     | 34.03 ± 0.09 | ±0.37  | 17  |
| SGB < 5   | 33.98 ± 0.06 | ±0.34  | 32  |
| All       | 34.02 ± 0.06 | ±0.43  | 58  |

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**Figure 17.** Galaxies in the Pisces filament sample in supergalactic coordinates. The location of the NGC 507 cluster is given by the large circle, that of A262 and the spotty north, is about normal. The luminosity–linewidth relation is seen in Figure 6(b).
In the case of the Pegasus Cluster, the one $2\sigma$ outlier (PGC 71159) is seen in Figure 18 to lie at the very center of the cluster, a circumstance that might suggest an anomaly. In the case of Cancer, Bothun et al. (1983) have convincingly shown that this region, as with Pisces and Ursae Major, is more complex than just a cluster. The circle in Figure 18 shows the location of the main concentration of galaxies identified from a redshift survey. Our sample is drawn from a more extended area. Regarding A400, A1367, and A2634 there is not much to be said. Figure 18 shows the sky distributions in each case. The scatter about the central cluster is somewhat greater with A1367 and reasonably confined with the other two. There are no anomalies in the luminosity–linewidth plots seen in Figure 6(b). A2634 is noteworthy as the significantly most distant cluster in this collection.

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Figure 18. Projection of six samples in supergalactic coordinates. In all of the panels the large circles approximate the second turnaround radii of the collapsed cores. In the case of the Coma sample the small dots show the distribution of a redshift sample while the large symbols identify the galaxies used in the template: open squares: cases that scatter $>0.4$ mag brightward of the mean relation; open triangles: cases that scatter $>0.4$ mag faintward. In the case of the Pegasus Cluster the open square identifies the location of PGC 71159, the most strongly deviant galaxy from the linewidth correlation.
