Quantum Tagging: Authenticating Location via Quantum Information and Relativistic Signalling Constraints

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We define the task of quantum tagging, that is, authenticating the classical location of a classical tagging device by sending and receiving quantum signals from suitably located distant sites, in an environment controlled by an adversary whose quantum information processing and transmitting power is unbounded. We define simple security models for this task and briefly discuss alternatives.

We illustrate the pitfalls of naive quantum cryptographic reasoning in this context by describing several protocols which at first sight appear unconditionally secure but which, as we show, can in fact be broken by teleportation-based attacks. We also describe some protocols which cannot be broken by these specific attacks, but do not prove they are unconditionally secure.

We review the history of quantum tagging protocols, which we first discussed in 2002 and described in a 2006 patent (for an insecure protocol). The possibility has recently been reconsidered by Malaney and Chandran et al. All the more recently discussed protocols of which we are aware were either previously considered by us in 2002-3 or are variants of schemes then considered, and all are provably insecure.

INTRODUCTION

There is now a great deal of theoretical and practical interest in the possibility of basing unconditionally secure cryptographic tasks on some form of no-signalling principle as well as, or even instead of, the laws of non-relativistic quantum theory. The earliest examples of which we are aware are bit commitment protocols based on no-signalling [1, 2], discovered in 1999-2000, which are provably secure against all classical attacks and against Mayers-Lo-Chau quantum attacks. The first secure quantum key distribution protocol based on no-signalling [3] was discovered in 2005. (See also Ref. [4] for some further details and discussion.) It has subsequently been significantly developed, producing more efficient protocols provably secure against restricted classes of attack [5-9] and then against general attacks [10-14]. A protocol for an interesting novel cryptographic task, variable bias coin tossing, using both quantum theory and the no-signalling principle, was published in 2006 [15]. Protocols for expanding a private random string, using untrusted devices, based on quantum theory and the no-signalling principle, were also recently introduced [16]; see [18] for a more complete presentation of this work) and significantly developed [17, 18]; note that at present the unconditional security of all these randomness expansion protocols against completely general attacks is an open question.

We define and discuss here another example of an interesting cryptographic task, quantum tagging, and present and discuss quantum tagging protocols which rely both on the properties of quantum information and on the impossibility of superluminal signalling.

QUANTUM TAGGING: DEFINITIONS

We work within a Minkowski space-time $M^{(n,1)}$, with $n$ space dimensions. The most generally applicable case is thus $n = 3$. The case $n = 2$ applies in scenarios where all parties are effectively restricted to a plane – for instance a small region of the Earth’s surface. The case $n = 1$ is physically realistic only if the agents are effectively confined to a line. Although this is unlikely in realistic applications, we will consider this case below, as it simplifies the discussion while illustrating many key points.

There are several distinct interesting security scenarios for quantum tagging, for example:
Security scenario I

Alice operates cryptographically secure sending and receiving stations $A_0$ and $A_1$, located in small regions (whose size we will assume here is negligible, to simplify the discussion) around distinct points $a_0$ and $a_1$ on the real line. The locations of these stations are known to and trusted by Alice, and the stations contain synchronized clocks trusted by Alice. Her tagging device $T$ occupies a finite region $[t_0, t_1]$ of the line in between these stations, so that $a_0 < t_0 < t_1 < a_1$. The tagging device contains trusted classical and/or quantum receivers, computers and transmitters, which are located in a small region (which again, to simplify the discussion, we assume is of negligible size compared with $(t_1 - t_0)$ and other parameters) around the fixed point $t_+ = \frac{1}{2}(t_0 + t_1)$. The device is designed to follow a protocol in which classical and/or quantum outputs are generated via the computer from inputs defined by the received signals. The outputs are sent in a direction, left or right (i.e. towards $a_0$ or $a_1$) that again depends on the inputs. The tagging device may also contain a trusted clock, in which case the clock time is another allowed input.\(^{[26]}\) Note however that it would not make sense in our scenario to assume from the start that the tagging device $T$ contains a trusted GPS device so that $T$ can verify and authenticate its own location. To analyse possibilities of this type, we would need to include the fixed GPS stations among Alice’s laboratories, and the communications between these stations and $T$ would form part of the tagging protocol.

We assume that signals can be sent from $A_i$ to $T$, and within $T$, at light speed, and that the time for information processing within $T$ (or elsewhere) is negligible. $T$ is assumed immobile and physically secure, in the sense that an adversary Eve can neither move it nor alter its interior structure. However, $T$ is not assumed impenetrable: Eve may be able to send signals through it at light speed, and may also be able to inspect its interior. In particular, $T$ contains no classical or quantum data which Alice can safely assume secret, and she must thus assume that its protocol for generating outputs from inputs is potentially public knowledge.

$T$ can be switched on or off. When switched off, it remains immobile and physically secure, and simply allows any signals sent towards it to propagate unmodified through it: in particular, signals travelling at light speed outside $T$ also travel through $T$ at light speed.

Eve may control any region of space outside $A_i$ and $T$, may send classical or quantum signals at light speed through $A_i$ and $T$ without $A_i$ or $T$ detecting them, may be able to jam any signals sent by $A_i$ or $T$, and may carry out arbitrary classical and quantum operations, with negligible computing time, anywhere in the regions she controls. Eve cannot cause any information processing to take place within $T$, other than the (computationally trivial) operation of transmitting arbitrary signals through $T$, except for the operations that $T$ is designed to carry out on appropriate input signals. Her task is to find a strategy which spoofs the actions of $T$, that is, makes it appear to $A_i$ that $T$ is switched on when it is in fact switched off. Conversely, $A_i$’s task is to design $T$, together with a tagging protocol with security parameter $N$, so that the chance, $p(N)$, of $E$ successfully spoofing $T$ throughout a given time interval $\Delta t$ obeys $p(N) \rightarrow 0$ as $N \rightarrow \infty$.

In this scenario, Eve is limited: she can neither move $T$ nor carry out non-trivial operations within the space it occupies. One could imagine that $T$ is tagging an object in a hostile environment which neither $E$ nor $A_i$ can enter. $E$ might, however, be able to destroy the object together with $T$ – thus effectively switching $T$ off – and spoof the tagging protocol so that $A_i$ is unaware of the loss.

Security scenario II

In scenario II, the tag is physically secure, but not immobile. Eve can move it, without disturbing its inner workings, at any speed up to some bound $v$, known to Alice. Clearly $v < c$, the speed of light, gives an absolute upper bound. To avoid considering relativistic effects, we assume $v \ll c$ here when we consider this scenario.\(^{[27]}\)

Practical relevance

As already noted, in realistic applications, $T$ would generally occupy a 3-dimensional region, $A$ might have any number of sending and receiving stations lying in different directions from $T$, and $T$’s outputs might be sent to any or all of these.

We envisage that in realistic applications $T$ would be a device securely attached to an object whose location is significant to $A$. In practice, we imagine, Eve might be able to destroy $T$, or move it along with the object to a region disjoint from that it originally occupies, and then replace it with another device. However, each of these operations would necessarily take some time, and we assume the relevant time can be bounded below by some minimum, $\Delta t$.\(^{[28]}\)
The idea of a tagging protocol is thus to ensure that any such interference by Eve would be detected by Alice before Eve’s operations are complete, because $T$ is not functioning as it should, according to the protocol, given its presumed location. Within a given security scenario, tagging protocols in which $A$ is attempting to verify that $T$ is stationary can easily be generalised to protocols in which $A$ is attempting to verify the location of $T$, when she knows that $T$’s speed will be bounded (with respect to a given frame, for example the stationary frame of Alice’s stations). We thus consider the case of verifying the location of a stationary $T$.

In this way, we separate the issues of $T$’s physical security and the security of its attachment to the object from specific aspects of its cryptographic security, defined by appropriate models. We analyse cryptographic security here via the security models given above. We would argue that, in a scenario in which all a tag’s operations are potentially visible to an adversary, a tagging protocol which is provably breakable in one of our models cannot be sensibly said to be unconditionally secure. To analyse the physical and other security issues in realistic applications, one needs further to consider how well – and under which assumptions – these models apply. We do not examine these latter issues further here (but see Ref. [22] for further discussion).

Other security scenarios and other models can also be considered, of course. Our aim here is to introduce the problem of quantum tagging and set out some interesting scenarios and questions, not to analyse all possibilities.

Spoofing

In a general spoofing attack on a tagging scheme, Eve intercepts some or all of the signals transmitted by $A$ and $T$ at one or more sites, carries out information processing on them at these sites, and retransmits the resulting outputs, which may be rerouted or delayed, to other sites under her control and/or to $A$ and/or $T$. Her information processing may involve collective operations on any information in her possession, including signals received directly from $A$ and $T$, ancillary information generated in her sites, and information generated by her own earlier operations.

For example, tagging schemes that do not rely on precise timings are vulnerable to simple record-and-replay spoofing attacks. In a record-and-replay attack, Eve intercepts all the outgoing signals from the tagging device, in a way that effectively jams the outgoing channel, preventing any signal reaching $A$ from $T$. Eve then replays the outgoing signals, unaltered, at later times, transmitted from different locations. By so doing she can hope to persuade $A$ that the device is in a given location when its location has in fact been altered: i.e., she can hope to render the scheme insecure under scenario II above.

Our aim is to discuss the possibility of devising protocols that use timed quantum (and perhaps classical) signals, together with relativistic signalling constraints, to ensure security against general spoofing attacks.

Types of input and output

We want to distinguish between input and output signals that carry classical information and those that carry quantum information. By the latter, we mean signals carried by a single quantum state lying in a fixed finite-dimensional Hilbert space — for example, a qubit. By the former, we mean a signal robust enough and redundant enough to be considered classical, that can be copied effectively infinitely and broadcast with effectively arbitrary fidelity, and that cannot practically be created in superposition: for example, a radio transmission.

Physics (as currently understood) provides no fundamental qualitative distinction between the classical and quantum. Any classical signal could be treated as a (perhaps very redundant) quantum signal, by considering a Hilbert space of suitably large dimension. Nonetheless it would be practically significant and cryptographically interesting to find a scheme that is secure if (but only if) some signals are considered classical.

To simplify the analysis a little, we characterise an input which involves both type of signals — for example, a classical input from one source and a quantum input from another — as a quantum input, and we characterise a quantum output similarly. This gives four distinct cases to consider: classical input and classical output (CC), quantum input and classical output (QC), classical input and quantum output (CQ), and quantum input and quantum output (QQ). Since CC and CQ schemes allow the input to be copied and broadcast, creating an immediate potential vulnerability, we focus here on QC and QQ schemes.
SOME SIMPLE INSECURE SCHEMES

The schemes we describe in this section are not perfectly secure. We nonetheless find them of practical and theoretical interest, since the only attacks to which we know they are vulnerable require advanced information technology that is presently unavailable (specifically, perfectly efficient implementation of quantum teleportation). We assume noiseless communication here: our discussion can be generalized to the noisy case by considering standard error correction methods.

Scheme I

Alice sends quantum signals, taking the form of a series of independently randomly chosen qubits, $|\psi_i\rangle$, from $A_0$, and classical signals, taking the form of a series of independently randomly chosen bits, $a_i$, from $A_1$. The qubits are chosen to be pure states, drawn randomly from the uniform distribution on the Bloch sphere. These signals are sent at light speed, timed so as to arrive pairwise simultaneously at $t_+$: that is, the first qubit and the first bit arrive together, then the second qubit and the second bit, and so on.

The tagging device $T$ interprets the classical bits as an instruction to send the qubit $|\psi_i\rangle$ in the direction of $A_0$ or $A_1$ (i.e. $a_i$ codes to send towards $A_{a_i}$). Upon receiving the bit and qubit, $T$ immediately obeys the instruction, redirecting the qubit in the appropriate direction. Alice tests that the qubits received at the receivers $A_i$ are the qubits she sent, and that they arrived at the appropriate times. (The first test is implemented by carrying out a projective measurement onto the space spanned by the originally transmitted qubit.) If this test is passed for $N$ successive qubits, sent within the interval $\Delta t$, she accepts the location of $T$ as authenticated.

Scheme II

Alice sends a sequence of pairs $(a_i,|\psi_i\rangle)$ from $A_0$, and a sequence $b_i$ from $A_1$. Here the $a_i$ are a sequence of independently randomly chosen numbers in the range $1 \leq a_i \leq m$, and the $b_i$ are a sequence of independently randomly chosen numbers in the range $1 \leq b_i \leq n$, while the $|\psi_i\rangle$ are independently randomly chosen qubits. The qubits are chosen to be pure states, drawn randomly from the uniform distribution on the Bloch sphere.

The signals $(a_i,|\psi_i\rangle)$ and $b_i$ are timed to arrive pairwise simultaneously at $t_+$. The $a_i$ and $b_i$ together code an instruction, defined by some previously fixed function $f(a_i, b_i) \in \{0,1\}$, to send the qubit to detector $A_0$ or $A_1$ respectively. [30] Immediately on receipt of the $i$-th set of signals, $T$ follows this instruction, redirecting the qubit towards $A_{f(a_i, b_i)}$. Alice tests that the qubits received at $A_i$ are the qubits she sent, and that they arrived at the appropriate times. (The first test is implemented by carrying out a projective measurement onto the space spanned by the originally transmitted qubit.) If this test is passed for $N$ successive qubits, sent within the interval $\Delta t$, she accepts the location of $T$ as authenticated.

Scheme III

Alice sends a sequence of independently randomly generated qubits $|\psi_i\rangle$ from $A_0$, and a sequence of independently randomly generated classical trits $c_i$ from $A_1$. The qubits $|\psi_i\rangle$ are chosen randomly from the set $\{|0\rangle, |1\rangle, |\pm\rangle, |\pm i\rangle\}$, where

$$|\pm\rangle = \frac{1}{\sqrt{2}}(|0\rangle \pm |1\rangle), |\pm i\rangle = \frac{1}{\sqrt{2}}(|0\rangle \pm i|1\rangle).$$

The trits, which are uniformly distributed, are interpreted as coded instructions to carry out a projective measurement in one of the bases $B_0 = \{|0\rangle, |1\rangle\}$, $B_1 = \{|+, |-\rangle\}$, $B_2 = \{|i\rangle, |-i\rangle\}$. These signals are sent at light speed, timed so as to arrive pairwise simultaneously at $t_+$: that is, the first qubit and the first bit arrive together, then the second qubit and the second bit, and so on.

As soon as the pair $|\psi_i\rangle$ and $c_i$ are received, $T$ measures $|\psi_i\rangle$ in the basis $B_{c_i}$. It then immediately classically broadcasts the measurement outcome bidirectionally. [31]

If the measurement statistics agree with those predicted by quantum theory, and the measurement results are received at the appropriate time by both detectors, for $N$ successive qubits, sent within the interval $\Delta t$, Alice accepts the location of $T$ as authenticated.
Comment on authentication and timing

For these schemes, and indeed any quantum tagging scheme in which Alice maintains laboratories at separated sites, it will of course take some time for her to collate and compare the data received at her various sites. Alice thus cannot possibly hope to authenticate, at any given time, that the tagging device is functioning correctly at that instant in time (in her lab rest frame). The aim of a quantum tagging protocol is rather to allow her to verify that the device was functioning correctly, at the correct location, within a given past fixed time interval (which necessarily lies in the past light cone of the point(s) at which verification is completed).

Discussion of (in)security of schemes I-III

An argument, which may seem plausible at first sight, suggests that schemes I-III should be unconditionally secure. We first review the argument, then explain why it is incorrect and show that the schemes are in fact insecure in either of our security models.

A naive security argument

Because quantum information cannot be cloned, the incoming qubits $|\psi\rangle$ must follow a unique path. If the qubits are transmitted directly to $T$, the required output data cannot be reliably generated at the correct time except by following the tagging protocol at $T$. If, on the other hand, the qubit is rerouted in some other direction, it encounters the classical data transmitted from $A_1$ at a later time than it would have if the tagging protocol were followed.

Since Eve does not know what to do with the qubit – which way to send it, or in which basis to measure it – until the classical data from $A_1$ arrive, she cannot be sure how to act until the classical and quantum data coincide. By this point, it is too late for them to be able to produce outputs that will arrive at the correct times at both $A_0$ and $A_1$. For example, in scheme I, if $E$ delays and stores the qubit somewhere between $A_0$ and $T$, and waits for the classical signal to arrive from $A_1$ before retransmitting the qubit, she can spoof the protocol if instructed to send the qubit to $A_0$, but cannot get the qubit to $A_1$ in time if instructed to send the qubit there.

Hence – the argument purports to show – on each round any spoofing attack has a nonzero probability of detection. Moreover, a nonzero lower bound for this probability can be calculated, and the tagging scheme is thus secure.

What’s wrong with the naive security argument?

One could try to formalise this naive argument as follows. Because of the no-cloning theorem, the quantum information encoded in the qubits $|\psi_i\rangle$ cannot be duplicated and so must follow a single definite trajectory. This would imply in particular that the quantum information must be localised at a single point at any given time.

While this might seem plausible at first sight, there are actually many ways in which quantum information can be delocalized. For example, $E$ could create a superposition of distinct trajectories via interferometry. Another possibility is that she could teleport the qubit and broadcast the classical information generated by the teleportation. These possibilities show that the naive security argument fails, since after these operations the quantum information encoded in the qubit no longer follows a single space-time path, at least in any standard sense. We now show that $E$ can indeed exploit the power of teleportation to break the above schemes.

Teleportation attacks on schemes I and II

As scheme I is a special case of scheme II, we need only consider the latter. Consider the following attack.

Eve sets up laboratories at sites $E_0$, between $A_0$ and $T$, and $E_1$, between $T$ and $A_1$. She arranges a sequence of labelled entangled singlet pairs to be shared between the sites $E_0$ and $E_1$, with labels $i$ (indicating which tagging signal a given set of pairs is going to be used to attack) and $j$ (which runs from 1 to $m$). When the signal $(a_i, |\psi_i\rangle)$ reaches $E_0$, Eve carries out a teleportation measurement with the incoming qubit and the first singlet qubit with label $(i, a_i)$. The classical teleportation data, describing the unitary operation needed to complete the teleportation, are immediately sent towards $E_1$ with a copy being kept at $E_0$. When the signal $b_i$ reaches $E_1$, Eve sends all the qubits stored there with labels $(i, a_i)$ for which $f(a_i, b_i) = 0$ towards the site $A_0$, using distinct physical degrees of freedom.
so that she can identify each qubit’s label $a_i$ at any later time. She stores at $E_0$ all the qubits with labels $(i, a_i)$ for which $f(a_i, b_i) = 1$, until receipt of the signal $a_i$. When the signal $a_i$ and the teleportation signal simultaneously reach $E_1$, if $f(a_i, b_i) = 1$, then Eve (at $E_1$) applies the teleportation operation to the stored qubit with label $(i, a_i)$ and transmits the teleported qubit towards $A_1$, discarding the remaining qubits from batch $i$ stored at $E_1$; if $f(a_i, b_i) = 0$ then Eve (at $E_1$) discards all the qubits from batch $i$ stored at $E_1$. When the signal $b_i$ and the transmitted qubits simultaneously reach $E_0$, if $f(a_i, b_i) = 0$, then Eve (at $E_0$) applies the teleportation operation to the transmitted qubit with label $(i, a_i)$, transmits this qubit towards $A_0$, and (at $E_0$) discards the others from batch $i$ stored at $E_0$; if $f(a_i, b_i) = 1$ she discards all the qubits from batch $i$ stored at $E_0$.

Eve attempts to ensure that none of her classical signals are detected by $A_0$ or $A_1$, either by transmitting them on frequencies not used by $A$ or by jamming her classical signals so that none is transmitted to the left of $E_0$ or the right of $E_1$. Eve allows Alice’s classical signals to propagate freely between $A_0$ and $A_1$ — i.e. she reads them but does not jam them.

Through this teleportation attack, Eve can spoof the tagging scheme and cause Alice to accept the location of $T$ as authenticated.

**Teleportation attacks on scheme III**

Eve sets up laboratories at sites $E_0$ and $E_1$, located as above. She arranges a sequence of labelled entangled singlet pairs to be shared between these sites, with labels $i$ (indicating which tagging signal a given set of pairs is going to be used to attack). When the signal $|\psi_i\rangle$ arrives at $E_0$ from $A_0$, she carries out a teleportation measurement at $E_0$. The classical teleportation data, describing the unitary operation needed to complete the teleportation, are immediately sent towards $E_1$, with a copy being kept at $E_0$. When the signal $c_i$ arrives at $E_1$ from $A_1$, she carries out a measurement in basis $B_{c_i}$ on the second particle from singlet $i$. The measurement outcome and basis are immediately sent towards $E_0$.

The teleportation unitary operations $I, X, Z, XZ$ leave the bases $B_0$, $B_1$ and $B_2$ invariant. Hence, from the outcome of a measurement in a basis $B_j$ ($j = 0, 1$ or $2$) on the unitarily rotated state $U|\psi_i\rangle$ represented by the second entangled qubit, together with a description of the unitary $U$, Eve can infer the outcome of the same measurement on the original state $|\psi_i\rangle$.

Thus, combining the classical signals from $E_0$ and $E_1$ at either site, Eve can infer the measurement outcomes required by the tagging scheme. By sending these outcomes immediately to the $A_i$, she can thus spoof the tagging scheme.

**SECURE TAGGING PROTOCOLS?**

The vulnerability of schemes I and II to the teleportation attacks described reflects a general weakness of QQ schemes in which the output is directed to a single detector. The attack described on scheme III reflects a specific weakness in the design of this scheme, arising from the fact that the measurement bases chosen are invariant under teleportation operations. This motivates considering variations on this scheme, such as the following examples.

**Scheme IV**

From $A_0$, Alice sends a sequence of random pure qubit states, drawn independently from the uniform distribution on the Bloch sphere. From $A_1$, she sends a classical signal selecting a random measurement basis, drawn independently from the uniform distribution on the set of Bloch sphere antipodes (i.e. uniformly distributed on some hemisphere). These states are sent to arrive simultaneously at $T$, which is instructed to carry out a measurement of the received qubit in the specified basis and then immediately to broadcast the outcome classically to both $A_0$ and $A_1$.

**Scheme V**

Clearly, scheme IV is idealized: a real implementation would select the qubit and basis from (perhaps very large) finite lists, approximating uniform distributions over the Bloch sphere. This can be done in infinitely many ways. Scheme V is one concrete and simple example, using a simplified version of scheme IV. It exploits the essential idea,
without attempting a good approximation of uniform distributions. From $A_0$, Alice sends random states drawn from the list $\{|0\rangle, |1\rangle, \cos(\pi/6)|0\rangle + \sin(\pi/6)|1\rangle, \sin(\pi/6)|0\rangle - \cos(\pi/6)|1\rangle\}$. From $A_1$, she sends random trits coding for measurements in the bases $B_0 = \{|0\rangle, |1\rangle\}$, $B_1 = \{\cos(\pi/6)|0\rangle + \sin(\pi/6)|1\rangle, \sin(\pi/6)|0\rangle - \cos(\pi/6)|1\rangle\}$, $B_2 = \{\cos(\pi/6)|0\rangle + i\sin(\pi/6)|1\rangle, \sin(\pi/6)|0\rangle - i\cos(\pi/6)|1\rangle\}$. The scheme then proceeds as above.

**Scheme VI**

Scheme VI is a variation of scheme IV, with an extra feature which may make the security of the scheme easier to prove (if indeed it is provably secure). The same idea can be used to define variations of scheme V or other schemes related to scheme IV.

From $A_0$, Alice sends random states $|\psi_i\rangle$ drawn independently from the uniform distribution on the Bloch sphere. The classical signal broadcast from $A_1$ sends a random measurement basis $b_i$ drawn independently from the uniform distribution on the set of Bloch sphere antipodes (i.e. uniformly distributed on some hemisphere) and two random bits $b_i, c_i$. These signals are timed to arrive simultaneously at $T$. If $b_i = 0$, this signal instructs $T$ to carry out a measurement in the basis $b_i$ (as in scheme IV) and report the result by a classical broadcast in both directions (again, as in scheme V). If $b_i = 1$, the signal instructs $T$ to send the (unmeasured) qubit $|\psi_i\rangle$ in the direction of $A_{c_i}$.

**Informal discussion of scheme VI**

The following informal comments give some motivation for considering scheme VI, but do not constitute a security proof.

The aim of this design is to use the possibility that $b_i = 1$ to prevent Eve from carrying out any form of teleportation-like attack in which classical information is extracted from the state $|\psi_i\rangle$. Such an operation would imply that $\psi_i$ cannot be reliably reconstructed later, which means that, if Eve performs it before she knows the value of $b_i$, she risks detection if $b_i = 1$. This ensures that Eve can only carry out teleportation-like operations which (like standard teleportation) ensure that the “teleported state” takes the form $U|\psi_i\rangle$, where $U$ is drawn from a finite list of possible unitary operations. The list must include operations other than the identity, since the density matrix of the “teleported state”, before reconstruction, is independent of $|\psi_i\rangle$. However, there is no non-trivial unitary operation which preserves all three bases $B_i$. This appears to leave Eve unable to carry out all the possible measurements required by the protocol without reconstructing the state (which cannot be done with the right timings, except by allowing the state to arrive at the tag $T$).

**Remarks on teleportation attacks**

Neither schemes IV and V share the vulnerability of scheme III to the specific teleportation attacks described above, since in both cases there is no non-trivial unitary operation that leaves all the relevant bases (the three specified bases in the case of scheme V, and the infinite set of all possible bases in the case of scheme IV) invariant.

One might further hope that the schemes are not vulnerable to general teleportation attacks, and more generally that they are indeed secure against all possible attacks.

Since the general set of operations that Eve might carry out is rather large, it would certainly be desirable if a security proof could be based on a specific counter-physical implication of the form “if Eve can spoof the tag, then it follows that they, perhaps in collaboration with Alice, can implement some physical operation known to be impossible”. An alternative proof strategy could be to identify sufficient constraints to show that Eve’s hands are effectively tied. One would hope to show (at least for schemes IV and VI, possibly also V) first that every possible operation that Eve can carry out is provably detectable unless it is a teleportation operation of a certain type, and then that such teleportation attacks are also provably detectable. (More precisely, one would like to prove both these claims with some lower bound on the probability of detection per spoofing attack.)

We offer no security proof of either type here.
More general schemes

Clearly, even in one dimension, the formulation of quantum tagging schemes allows a plethora of options. Alice could send both classical and quantum information from both stations $A_0$ and $A_1$; the quantum information sent from $A_0$ and $A_1$ in any given round could be entangled, as could the quantum information used in successive rounds; she could require any classical and quantum computation at $T$ that takes inputs of the prescribed form and produces two (possibly entangled, possibly both classical and quantum) output states to be returned to her sites.

It would be very interesting to understand precisely which levels of security can be attained by which types of tagging scheme, and how efficiently this can be done in each case. At present, to the best of our knowledge, these are open problems.

BRIEF HISTORY

The possibility of quantum tagging protocols was first considered by one of us (AK) in 2002. The six protocols presented here, together with the teleportation attacks on the first three, were variously invented and discussed by us during 2002-3. A patent for a quantum tagging protocol (which is not unconditionally secure, but appears unbreakable by present technology), based on notes filed for HP Labs Bristol in 2002, was granted and published in 2006.

Recently, other authors have considered the possibility of quantum tagging, and rediscovered some of the insecure protocols presented here, but apparently not the attacks on these protocols. Refs. argue, incorrectly, that their protocols are in fact secure. The protocol in Ref. is a simpler version of Scheme III above, which we considered in 2002. It is breakable by the teleportation attack on scheme III described above. The protocol in Ref. is a variation of a Bell state measurement scheme which we also considered in 2002. It is similarly breakable:

Eve can intercept and store the two particles comprising quantum states $|\Gamma_{iAB}\rangle$ at sites equidistantly located either side of $T$, apply the unitaries $(U_{iA}^A)^\dagger$ and $(U_{iB}^B)^\dagger$ to the respective states as soon as the classical signals arrive at her sites, use teleportation to carry out a non-local Bell state measurement on the resulting states, transmit the classical outcome data between her sites, calculate the measurement result at both sites, and transmit the result to $A$ and $B$ so as to arrive at the expected times.

NOTE ADDED

Some time after this work was circulated on the physics arxiv, papers developing further the results reported here were circulated by Kent, Lau and Lo and Buhrman et al. Ref. shows that unconditionally secure quantum tagging is possible in a scenario in which the tag is assumed to contain private data inaccessible to adversaries. Buhrman et al. show that schemes IV-VI, whose security was left as an open question above, are insecure against eavesdroppers with unbounded predistributed entanglement.

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In practice, whether Eve succeeds in this may depend on the technology available to her and Alice. However, for the protocol to be unconditionally secure, we require that an Alice whose signal detection power is bounded must be able to detect a spoofing attack by an Eve whose signalling technology is unbounded.

They may map one basis state to the other, but the unordered set containing the pair of states is left unchanged.