Determination of serviceability limits of a turboshaft engine by the criterion of blade natural frequency and stall margin

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Abstract. This paper analyses the health and performance of 12-stage axial compressor of the TV3-117VM/VMA turboshaft operated in a desert environment. The results of the dimensional control of 4,800 worn blades are analysed to model the wear process. Operational experience is used to assess the effectiveness of an Inlet Particle Separator. Numerical modal analysis is performed to generate the Campbell diagram of worn blades and identify resonant blade vibration which can lead to high cycle fatigue (HCF). It is shown that the gradual loss of the stall margin over time determines the serviceability limits of compressor blades. Recommendations setting out go/no-go criteria are made to maintenance and repair organisations.

1 Introduction

Long-term engine performance in adverse operating conditions is one of the main conditions for successful helicopter missions. Unlike an aeroplane, the helicopter has to hover for a long time above the ground, often raising cloud dust and causing a brownout. Therefore, the ability to conduct long-term operations at elevated dust concentrations is one of the most important features of modern helicopters. Studies on the impact of environmental particles on the efficiency of helicopter engines were already carried out during the development of the first types of helicopters [1].

The operation of a helicopter engine in a dusty environment causes contamination of the gas path [2, 3]. Deposition of particles on aerofoils [4, 5] and the heat exchanging surfaces of the air cooling system [6] can lead to deterioration of the aerodynamic and thermodynamic properties of these components. Moreover, given that dust particles (no matter how small they are) have abrasive properties, they also cause erosive wear of the engine components and contribute to various types of structural damage [7–9]. Erosive wear of compressor blades leads to reduction in the stall margin of the compressor, increase in the likelihood of fatigue damage of compressor blades due to changes in their natural frequencies of vibration and a decrease in the efficiency of the engine due to the wear of the gas path.

Rotating components are sensitive to mechanical damage caused by solid particles. The models describing their impact and related erosive damage were proposed by many researchers, such as Finney [10], Bitter [11] and Sheldon [12], but the prediction of the actual aerofoil degradation is still difficult. The main factors affecting the magnitude of erosion consist of the angle of collision, velocity and particle size, blade surface properties, and particle concentration. Van der Walt [13] showed that the wear rate of the aerofoils is directly proportional to dust concentration. The mechanical properties of the material are also an important parameter influencing the mechanisms of erosion [14, 15].

Eustyfeev [16] performed experimental and theoretical studies of compressor blades eroded by solids to determine the erosion resistance of the blade material EI-961. The limiting ratio of the
particle size to their velocity of contact with the material was determined. But the experiment was performed on a cut-out sample, not on a real blade, as well as on one type of material that is EI-961 steel, while most of the blades of modern compressors are made of titanium alloy.

Batcho [17] and Singh [18] analysed loss of performance caused both by erosion and deposition. The impact of ingested particles engine operation depends on the physical and chemical properties of the dust, its composition and concentration. Particles deposited on compressor aerofoils, change their geometry and roughness, which leads to a decrease in the efficiency and consequently reduce the pressure ratio and performance of the compressor [19].

The time between overhauls (TBO) of an engine operated in a highly dusty environment is much less than that set by the manufacturer and is reduced by the erosion of the compressor blades. The statistical analysis [20] showed that erosive wear of compressor blades was the cause of 30 - 35% of the engines grounded due compressor blade damage, the largest of all causes. This is comparable to the proportion of engine removals due to foreign objects ingested from the runway during take-off (25 - 30%). The share of aviation incidents, bird ingestion, or human errors during maintenance accounts for 15 - 20%.

The aim of this study was to assess the serviceability limit of the blades of the axial compressor of a helicopter engine operating in a dusty environment. To achieve this goal, the following tasks based on the results of the dimensional control of worn blades were performed:

- establishing patterns of blade wear as a function of flight hours (FH) and dust concentration
- evaluating the increase of the natural frequency of blades by modelling the geometry of worn aerofoils over the engine operating time
- development of a methodology for modelling the flow through the axial compressor
- calculating the compressor maps describing the blades with different degrees of wear

2 Methods

In this work, the compressor blades of the TV3-117 turboshafts powering the Mi-8MTV and Mi-24 helicopters helicopters in the desert environment of the Republic of Algeria are studied. The region of North Africa and the Middle East features, in addition to extreme ambient temperatures, a high concentration of dust and sand dispersing up to a height of 6000 m which is the helicopter operation zone. For example, in North Sudan, the dust concentration is 1.3 g/m³, and in Algeria 1.3 - 1.6 g/m³. The size of particles ingested into the gas path varies from 0.01 to 2 mm.

The operation of gas-turbine engines in the regions described above, with a high content of dust and sand, inevitably leads to deterioration of engine performance [21, 22]. Particles carried by the air may cause substantial erosive wear of compressor blades. A consequence of this is a widening of the tip clearance and a modification of the aerofoil profile - in particular, the chord length and the blade thickness appear to decrease, especially above 66% of the span. This leads to reduction in compressor pressure ratio and ultimately a reduction in efficiency of the entire engine.

Firstly, a statistical analysis is carried out to study the nature of compressor wear and to determine its critical components. Based on the subsequent regression analysis, patterns of wear of the blades of all compressor stages as a function of engine operation time and dust concentration are established.

The obtained patterns of the chord wear of blades of the all compressor stages are used to predict their geometry, depending on engine operating time. This allows us to model blade vibration and flow through the worn compressor, necessary for the determination of the serviceability limit of the blades in terms of structural integrity and the stall margin.

For the analysed engines, the observed impact of erosion on compressor performance was several times greater than deposition, due to a high dust concentration and fair inlet protection. Moreover, compressor fouling can be reversed by washing. Therefore, particle deposition is not taken into account in this work.

2.1 Blade inspection

The inspected engines were grounded and torn down for one of two reasons: either due to the chord wear of the compressor blades of the first stage in the upper part exceeding 2 mm; or, due to the performance parameters of the engine, such as the gas generator speed $n_1$ or the turbine inlet temperature TTT, being outside the permissible limits.
The dimensional control of blade geometry was performed by measuring the chord and the thickness of the profile at various sections as well as blade height. Ten blades were selected for the evaluation from each stage of 40 engines [23]. In total, 4,800 blades were inspected. Statistica 12 was used to analyse the results.

The inspected engines were initially divided into two categories. The former included those that were operated without a particle separator (IPS) and the latter with an IPS.

2.2 Structural analysis

Compressor blades of modern turboshafts are characterised by thin profiles and relatively low stiffness, therefore forced vibration represents a notable threat to them [24, 25]. The compressor blades absorb intense static and dynamic loads. When rotating under large centrifugal forces, the blades undergo deformation, which leads, in particular, to a decrease in their twist. The compressor blades vibrate due to unsteady flow forces relative to their static deformations. The distribution of dynamic stresses in blades has been determined to ensure that they are below the fatigue limit of the material [26, 27].

The erosive wear of blades has a significant impact on their strength, which is confirmed by the works of Hamed [1, 28]. The properties of the blade surface and its ability to withstand erosion are one of the key factors that determine the reliability of the system, since a variety of surface irregularities can lead to stress concentration that increases the risk of high cycle fatigue (HCF) [29–32].

The main reason for the excitation of blade vibration is circumferential flow irregularity. The flow is also non-uniform in the radial direction. The frequencies of the driving forces are multiples of the rotor speed (engine orders) which are equal to the number of obstacles around the circumference e.g. the number of guide vanes and struts in the gas path. When the speed changes, a number of resonant frequencies can be excited. To predict the frequencies of resonant vibration, a modal analysis of blades and the Campbell diagram are necessary [33, 34].

Vibration frequencies and operational deflection shapes with a certain degree of accuracy can be determined by numerical methods, in particular using volumetric finite element models (FEM). To date, this research method is preferred, since the complex geometry of the aerofoils is generally not amenable to the analytical method of calculating frequencies and vibration modes.

Blade geometry was measured using an 3D scanning, followed by postprocessing in the CAD system ASCON KOMPAS 16.0. Geometry models of compressor blades were developed in Unigraphics NX8. To describe compressor blades after various periods of operation in a dusty environment, parameterized solid-state models were used. By varying blades height, chord length and thickness in the corresponding sections of the aerofoil, several variants of blade geometry were generated.

The grid models of blades, developed using the ANSYS ICEM CFD grid generator, consisted of 15 - 18 thousand hexagonal elements SOLID 185. The calculation of the natural vibration frequencies of the blades was carried out numerically using the ANSYS 14.5 solver.

2.3 CFD model

The 3D flow calculation, with an ideal gas as the working fluid, was based on the Navier-Stokes equations and the finite element method (FEM), implemented in the ANSYS CFX solver. The mesh was developed in ANSYS Turbo Grid to model the operation of all stages. A separate mesh flow model (domain) was designed for each blade. The following grid parameters were considered when building the grid:

- **ATM Optimized topology** provides a high quality mesh, hexahedral elements, twisted aerofoils
- **Parameter y+ size** of the first wall element has a value within (80-160) units
- **The ratio of the dimensions of the elements does not exceed 6.**

Firstly, the flow calculation was performed for two rotational speeds of the compressor rotor 95% and 98%, where 1% corresponds to 195.37 rpm. Ambient air temperature 288 K and pressure 101.325 kPa was assumed. Each rotational speed of the compressor rotor corresponds to certain angles of variable inlet guide vanes (IGV) and guided vanes of the further four stages.

To reduce the required computing power, a single blade with cyclic symmetry along the lateral boundaries of the domain was modelled for each compressor stage. Stage interfaces (Mixing-Plane) between fixed and rotating domains were defined, which enables interpolation between interconnected grids, taking into account the laws of mass conservation.
The choice of the turbulence model depends on the nature of the turbulent flow, the required accuracy, the available computational resources, and the time cost. The SST K-ω turbulence model of Mentera was chosen as more accurate and reliable for the class of flows with a positive pressure gradient. The residual RMS error of $1 \times 10^{-6}$ was assumed as the satisfactory condition of CFD convergence and it was achieved after 600-870 iterations.

CFD results were used to estimate the compressor maps, as in another paper about this turboshaft [35]. The mass flow rate was measured at the outlet of the compressor. Each operating point corresponded to a certain mass flow, in the range from 4 to 11 kg/s.

3 Results and discussion

3.1 Chord wear

The results of the dimensional control of the compressor blades show that the highest wear is observed at the blade tip, while a much lower wear is exhibited near the root (Figure 1). The chord wear of the sections 2 - 4 can be expressed as a function of the wear of the tip section.

![Figure 1. Chord wear of the compressor blade in specific cross-sections](image)

Statistical analysis carried out for individual stages revealed the wear patterns caused by the design features of the compressor. Figure 2 shows the chord wear of the compressor blades of all the stages. For engines operated without IPS, the largest wear is observed for the first-stage blades while for engines operated with IPS is is for the sixth stage blades.

Engines belonging to the first category, operated without IPS, were grounded in accordance with the current standards for the maximum allowable wear of the chord of the blade of the first stage of the compressor in the upper part: 2 mm. The effective TBO of the first category engines was only 150 - 200 FH, provided that it nominally is 1500 FH for this type of engine.

Engines from the second category, operated with IPS, were removed from service due to their operating parameters, such as the $n_1$ speed and the turbine inlet temperature, beyond the permissible limits. The effective TBO for the second category was 600 - 650 FH what indicates a partial effectiveness of the applied IPS [36].

Given the close correlation ($R > 0.856$) between the wear of the blades of the stages 2-12, it is possible to assess the wear of the blades of each stage based on the established regression dependencies. As the independent variable, the chord wear of the sixth stage blades is used. This choice is explained by the fact that, despite the obvious advantages of using the first stage for the dimensional control of blades, which are the most convenient from the point of view of monitoring and predicting remaining useful life (RUL) without removing and disassembling the engine, it does not correlate well with the wear of the remaining stages ($R < 0.4$).

The chord wear of the compressor stages 2-12 correlates with the wear of the sixth-stage blades and can be estimated using the linear regression.

$$c_i = a_i c_6 + b_i$$  \hspace{1cm} (1)
The dependence of the chord wear on the engine operating time in a dusty environment can be satisfactorily described by a second-order curve (Figure 3).

\[ c_6 = (4.69 \times 10^{-6} t + 1.25 \times 10^{-3}) t \delta \]

where \( \delta \) is the dust concentration in g/m³. For the analysed fleet, the average concentration \( \delta = 1.6 \) g/m³ can be assumed:

\[ c_6 = 7.5 \times 10^{-6} t^2 + 0.02 t \]

**Figure 2.** Histogram of chord wear of the compressor blades of individual stages, for an engine without IPS; b with IPS

**Figure 3.** Chord wear of sixth-stage blades in function of flight hours

### 3.2 Modal analysis of blades

To assess the effect of wear on the natural frequency of the vibration, a modal analysis was performed. For each stage, an individual Campbell diagram was developed taking into account the nominal and worn profile of the aerofoil. Erosion significantly increases the natural frequencies of the blades. The analysis reveals several resonances excited by engine orders. Some stages were identified for which there is a risk of resonance in the operating speed range (Figure 4).

The stages and the modes for which the risk of resonance is identified:

- **M7** of the first stage resonates with the EO30 due to the number of the inlet guide vanes. This resonance is possible at 4 mm chord wear in the upper part
- **M8** of the fourth stage resonates with the EO60 due to the number of the guide vanes of this stage. Resonance occurs when the chord wear equals 6.3 mm
3.3 Stall margin analysis

To assess the effect of erosion on the compressor performance, the flow was calculated for the nominal (initial) geometry of the blades, as well as the geometry corresponding to the engine operating time of 200, 400, 600, and 800 FH [23].

The compressor pressure maps (Figure 5) and efficiency maps (Figure 6) calculated as a function of flight hours shows that with increasing intensity of blade wear, the pressure ratio and its efficiency decreases. The stall margin (SM) is also reduced (Figure 6) and was calculated in accordance with equation:

$$\text{SM} = 100\% \left( \frac{\pi_{\text{stall}}}{\dot{m}_{\text{stall}}} - 1 \right)$$

where $\pi_{\text{stall}}$ is the pressure ratio for the stall line, and $\pi_{\text{ss}}$ is the pressure ratio for the steady state line.

A decrease in the stall margin of the compressor by 15% causes the appearance of a surge during test-cell testing of TV3-117 engines. The analysis of the mass flow in the high speed region for a compressor with blades with different degrees of wear showed that due to erosive wear in the upper parts of the blades of the stages 6-9, the compressor develops a stall, leading to surge. The reason for this phenomenon was a decrease in the chord of the blades and an increase in the radial clearance. For that reason, the compressor operated in a dusty environment reaches its serviceability limit after 730 - 750 FH.

4 Conclusions

Based on the analysis of the geometry of the compressor blades of the TV3-117 engines operated in a dusty environment it was found that the wear of the blades of all the compressor stages occurs uniformly. When the particle separator is used, the largest wear is observed for the blades of the stages 1-6. It is also established that there is a close correlation between the wear of the blades of the sixth stage and the stages 2-12.

An original method was developed to assess the influence of erosive wear of the blades and vanes on the compressor performance by modelling three-dimensional flow for various degrees of wear on the blades of all stages. The methodology for measuring the chord wear of the blades, calculating the natural frequencies of vibration taking into account the aerofoil wear, numerical calculation of the compressor flow and analysing the onset of stall, the use of which, in combination with established patterns of chord wear over engine operating time enabled the assessment of the serviceability limits of the blades.
Conclusions

Chord wear over engine operating time enabled the assessment of the serviceability limits of the blades. The methodology for measuring the chord wear of the blades, calculating the natural frequency, the compressor performance by modelling three-dimensional flow for various degrees of wear on the blades of all stages. It is also established that there is a close correlation between the wear of the blades of the sixth stage and the stages 2-12. Based on the analysis of the geometry of the compressor blades of the TV3-117 engines operated in a dusty environment it was found that the wear of the blades of all the compressor stages occurs in a dusty environment. The stall margin (SM) is also reduced (Figure 6) and was calculated in accordance with the criterion of stall margin of the TV3-117 turboshaft. The chord wear of the sixth-stage blades decreases. The stall margin (SM) is also reduced (Figure 6) and was calculated in accordance with the criterion of stall margin of the TV3-117 turboshaft. The chord wear of the sixth-stage blades decreases. The stall margin (SM) is also reduced (Figure 6) and was calculated in accordance with the criterion of stall margin of the TV3-117 turboshaft.

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The values of the maximum permissible chord wear of the blades of all stages are determined by the criterion of stall margin of the TV3-117 turboshaft. The chord wear of the sixth-stage blades equal 6.19 mm is critical because it is accompanied by a decrease in the stall margin of the compressor by 15-17% which indicates the appearance of a permanent stall at 770-790 FH. An additional slot for the optical inspection of the sixth stage was designed to enable field maintenance. The values of the maximum permissible chord wear of the blades of all stages are determined by the criterion of stall margin of the TV3-117 turboshaft. The chord wear of the sixth-stage blades equal 6.19 mm is critical because it is accompanied by a decrease in the stall margin of the compressor by 15-17% which indicates the appearance of a permanent stall at 770-790 FH. An additional slot for the optical inspection of the sixth stage was designed to enable field maintenance. 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