Broadband and Wide Field-of-view Plasmonic Metasurface-enabled Waveplates

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Quasi two-dimensional metasurfaces composed of subwavelength nanoresonator arrays can dramatically alter the properties of light in an ultra-thin planar geometry, enabling new optical functions such as anomalous reflection and refraction, polarization filtering, and wavefront modulation. However, previous metasurface-based nanostructures suffer from low efficiency, narrow bandwidth and/or limited field-of-view due to their operation near the plasmonic resonance. Here we demonstrate plasmonic metasurface-based nanostructures for high-efficiency, angle-insensitive polarization transformation over a broad octave-spanning bandwidth. The structures are realized by optimizing the anisotropic response of an array of strongly coupled nanorod resonators to tailor the interference of light at the subwavelength scale. Nanofabricated reflective half-wave and quarter-wave plates designed using this approach have measured polarization conversion ratios and reflection magnitudes greater than 92% over a broad wavelength range from 640 to 1290 nm and a wide field-of-view up to ±60°. This work outlines a versatile strategy to create metasurface-based photonics with diverse optical functionalities.

Optical metasurfaces are a new class of quasi two-dimensional metamaterials composed of a single layer of metallic nanostructures that provide exceptional capabilities for manipulating light in an ultrathin, planar platform1–3. In comparison to their three-dimensional counterparts, metasurfaces also exhibit reduced loss and fabrication complexity, making them attractive for integration in practical optical systems4. By engineering the geometry of the nanostructured metasurfaces, the spectral and spatial dispersion of their optical response can be tailored to generate a specific abrupt interfacial phase change and cross-polarized response on a subwavelength scale. Such unique optical properties have been exploited to demonstrate a variety of new physical phenomena and associated optical devices over the past few years, including anomalous reflection and refraction5–8, optical wavefront manipulation9–11, frequency-selective near-perfect absorption12–14, spin-hall effect of light15,16, spin-controlled photonics17, polarization-dependent unidirectional surface plasmon polariton excitation18,19, and metasurface holograms20–21.

Optical waveplates that achieve broadband polarization conversion with a wide field-of-view (FOV) are highly desirable for systems that perform optical characterization, sensing, and communications functions22. However, simultaneously achieving broadband and wide-angle properties is difficult using conventional multilayer stacks of birefringent materials because these structures rely on the dispersive properties of the birefringence. In contrast, metasurfaces provide a promising pathway towards broadband and wide-angle polarization conversion in a submicron-thick layer. A variety of optically thin, metasurface-based polarization-control components have been theoretically proposed and demonstrated, including various polarizers23,24, near-field polarization shapers25, and ultrathin waveplates26–34.

Most metasurface-based waveplates have employed homogenous arrays of weakly coupled anisotropic resonant building blocks, including crossed nanodipoles24,28 and nanoslits27–29, L-shaped30 or V-shaped31 nanoantennas, and elliptical nanoholes32. These structures typically suffer from a narrow FOV, limited bandwidth, and/or low efficiency because their anisotropic optical response relies on the resonance of each isolated building block, where strong dispersion and impedance mismatch may exist. More recently, a near-infrared (IR) quarter-wave plate achieved broadband circular-to-linear polarized light conversion by tailoring the dispersive properties of an array of orthogonally coupled nanodipole elements. However, the waveplate had an average power efficiency of less than 50%.35 In addition, to obtain broadband circularly polarized transmitted light from this design, incident linearly polarized light with a wavelength-dependent electric field polarization direction was required. An
alternative inhomogeneous metasurface design strategy has also been used to produce an ultrathin broadband quarter-wave plate\(^\text{39}\). The demonstrated design achieves a power efficiency of only 10% over a narrow FOV, and has a wavelength-dependent directivity of the outgoing polarization.

In this paper, we demonstrate wide-angle reflective plasmonic metasurface-based half-wave and quarter-wave plates that have a high polarization conversion efficiency and reflection magnitude over a broad bandwidth in the visible-to-near IR wavelength range. This is achieved by optimizing the anisotropic optical response of the metasurface, which is composed of an array of strongly coupled nanorod resonator building blocks with controlled aspect ratio, to tailor the spectral dispersion of light interference between the metasurface and a metallic reflector. In contrast to previously reported metasurface waveplates, the anisotropic optical response and light interference are controlled across the broad wavelength range and wide-FOV rather than merely near the resonant wavelength of the metasurface building blocks. Both the nanofabricated half-wave and quarter-wave plates achieved measured polarization conversion ratios (PCRs) higher than 92% over more than an octave bandwidth from 640 nm to 1290 nm with a wide field-of-view of \(\pm 40^\circ\). This work represents a new state-of-the-art for optical metasurface-based devices, and will enable other types of ultrathin optical components with broad operational bandwidth, wide FOV and high efficiency.

Results

Structure and operation of reflective plasmonic metasurface-based waveplate. Figure 1a shows a simplified schematic of our metasurface-based waveplate that is used for simulation. The multilayer structure comprises a top homogeneous anisotropic metasurface, an intermediate silicon dioxide (SiO\(_2\)) layer separated from the metasurface by a subwavelength air spacer, and a bottom continuous gold (Au) layer. The metasurface is characterized by uniaxial surface polarizability tensors \(\chi_E\) and \(\chi_M\)\(^\text{35}\). Because the metasurface has no magnetic component and is modelled as an infinitely thin sheet, the surface polarizability tensors can be simplified to \(\chi_E = \text{diag}[\chi_{E,x}, \chi_{E,y}, \chi_{E,z}]\) and \(\chi_M = \text{diag}[0, \chi_{M,x}, \chi_{M,z}]\). The air layers above and below the metasurface are included in the design to account for the small phase retardation present in the fabricated nanostructure that has a finite thickness of \(l_{\text{m}} = \lambda_{90}/30\). The value of the phase retardation can thus be approximated by \(\phi \approx \theta_{\text{ph}}/2\).

The operating principle of the metasurface-based waveplate is illustrated in Figure 1b, and resembles that of a modified Gires-Tournois (G-T) etalon\(^\text{36}\). Here, a plane wave with prescribed polarization illuminates the multilayer structure from an incident direction \((\theta_i, \phi_i)\), where \(\theta_i\) denotes the angle between the z-axis and \(k_i\), while \(\phi_i\) is the angle formed by the x-axis and the projection of \(k_i\) on the x-y plane. When the incident wave interacts with the multilayer structure, both s- and p-polarized reflected and transmitted waves are generated by the metasurface. The transmitted waves undergo multiple reflections between the metasurface and the bottom Au layer, where they interfere with one another to create the final reflected wave. Due to the anisotropy of the metasurface, both co-polarized and cross-polarized reflected waves are collected at the direction \((\theta_s, \phi_s-180^\circ)\). The dielectric spacer and the Au ground plane increase the design degrees of freedom for controlling the amplitudes and phases of the waves produced by the multiple reflections, and thus can be optimized to increase the bandwidth of the anisotropic reflection from the three-layer nanostructure. The complex reflection coefficients that describe the polarization-dependent optical response of this structure \((r_{sp}, r_{ps} = r_{pp}, r_{ps})\) can be calculated analytically using an interference model\(^\text{37}\) (details available in Supplementary Information, Eq. S1a to S1d). By tailoring the dispersive anisotropy of the metasurface as well as the interference of the s- and p-polarized wave components, the polarization state of the final reflected wave is controlled over a broad spectral and wide angular range.

Anisotropic optical response of the metasurface nanorod building blocks. The desired anisotropic homogenous metasurface can be realized using a single-layer metallic nanoresonator array provided that its periodicity is much smaller than the wavelength of interest\(^\text{1}\). As shown in Figure 1a, we employed a 2D array of Au nanorod building blocks with strong inter-element coupling because the dimensions and inter-element spacing of this simple geometry can be: (1) optimized to provide a widely varying anisotropic response, and (2) scaled to fabricate devices that operate at visible wavelengths. Before designing nanorod-based metasurfaces with the uniaxial surface polarizability properties required for our quarter-wave and half-wave plate devices, the optical properties of both isolated and strongly coupled pairs of Au nanorods were determined for a normally incident linearly polarized wave with its electric field either parallel or perpendicular to the long axis of the rod (Fig. 2a).

Figure 2c plots the calculated amplitude (normalized) and phase of the scattered light from a single nanorod with a length \(a_r = 250\) nm, a width-to-length aspect ratio \(a_r/a_z = 0.3\), and a thickness \(l_{\text{m}} = 30\) nm as well as a strongly coupled pair of nanorods with an inter-element gap \(g = 20\) nm. The electric fields are concentrated at the ends of the isolated nanorod (Fig. 2b), resulting in an x-directed dipolar resonance at \(930\) nm with a scattering phase of around \(90^\circ\). The localized surface plasmon polariton (LSPP) mode causes the nanorod to resonate at a wavelength much larger than twice its length. In contrast, for a pair of strongly coupled nanorods, the enhanced electric fields are effectively confined within the air gap between the two rods (Fig. 2b). The capacitance formed in the air gap between the nanorods is much larger than the capacitance at the two ends of each individual nanorod\(^\text{38}\), resulting in an x-directed LSPP dipolar resonance occurring at \(1125\) nm, which is only 21% larger than the resonating wavelength of the single nanorod. This resonance also has a lower quality factor as demonstrated by the flatter phase response. For the mode corresponding to y-polarized incident

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*Figure 1 | Schematics of the proposed plasmonic metasurface-based waveplates. (a) 3D view of the multilayer structure model including an anisotropic homogenous metasurface located at a distance of \(r_{em}/2\) above the SiO\(_2\) layer. The metasurface is characterized by electric and magnetic surface polarizability tensors \(\chi_E\) and \(\chi_M\). Optically thin strongly-coupled nanorod array is used to realize the metasurface. (b) Interference model for evaluating the optical response of the multilayer structure based on the surface polarizability tensor parameters of the metasurface.*
illuminating a single nanorod or a pair of coupled nanorods. The dimensions are $D_w$ and $D_t$ (Fig. S3), which provides a percentage bandwidth of 62% for oblique angles of incidence (see Supplementary Information, Fig. S2).

The behavior causes a large phase difference over the broad wavelength region between the two orthogonally polarized resonating modes even at oblique angles of incidence (see Supplementary Information, Fig. S3), which provides a percentage bandwidth of 62% for phase difference $\Delta \phi > 90^\circ$ and 39% for $\Delta \phi > 135^\circ$. This is central to achieving broadband metasurface-enabled polarization transformations. To understand the effect of the nanorod structure on the phase of the scattered light, we first evaluated the phase difference as a function of length ($a_x$) and aspect ratio ($a_y/a_x$) of a single isolated rod was varied with all other parameters remaining unchanged. As shown in Fig. 2a, increasing the length and decreasing the aspect ratio both broaden the bandwidth of the large $\Delta \phi$ region, which is indicative of the degree of scattering anisotropy. For the strongly coupled nanorod pair, the data in Fig. 2d also demonstrates that the bandwidth of $\Delta \phi$ increases exponentially as the gap size drops due to the large increase in air gap capacitance of the structure. It should be noted that even though the nanorod building block has a wavelength-dependent scattering magnitude, all of the incident waves will be reflected by the bottom solid Au layer. By designing the nanosstructure such that it is operating away from its absorption band, the reflection magnitude for both polarizations will possess a flat response.

For the nanorod structure in Fig. 2a, the anisotropic scattering behavior causes a large phase difference over the broad wavelength region between the two orthogonally polarized resonating modes even at oblique angles of incidence (see Supplementary Information, Fig. S2 and S3), which provides a percentage bandwidth of 62% for phase difference $\Delta \phi > 90^\circ$ and 39% for $\Delta \phi > 135^\circ$. This is central to achieving broadband metasurface-enabled polarization transformations. To understand the effect of the nanorod structure on the phase of the scattered light, we first evaluated the phase difference as a function of length ($a_x$) and aspect ratio ($a_y/a_x$) of a single isolated rod was varied with all other parameters remaining unchanged. As shown in Fig. 2d, increasing the length and decreasing the aspect ratio both broaden the bandwidth of the large $\Delta \phi$ region, which is indicative of the degree of scattering anisotropy. For the strongly coupled nanorod pair, the data in Fig. 2d also demonstrates that the bandwidth of $\Delta \phi$ increases exponentially as the gap size drops due to the large increase in air gap capacitance of the structure. It should be noted that even though the nanorod building block has a wavelength-dependent scattering magnitude, all of the incident waves will be reflected by the bottom solid Au layer. By designing the nanosstructure such that it is operating away from its absorption band, the reflection magnitude for both polarizations will possess a flat response.

Most previously demonstrated plasmonic metasurfaces have been designed by optimizing the geometry of the single isolated resonant building block. This investigation reveals that strong inter-element coupling plays a critical role in controlling the scattering phase difference for achieving the tailored anisotropic optical dispersion required for broadband, low-loss performance. As discussed in the following sections, the bandwidth broadening due to inter-element coupling can be further enhanced when the strongly coupled nanorods are arranged in a 2D array.

Optimized broadband and wide-angle metasurface-based half-wave plate. Broadband and wide-angle plasmonic metasurface-based waveplates can be efficiently designed by using the interference model of the multilayer structure and the optical properties of the strongly coupled nanorod array. As a proof-of-concept, here we consider a half-wave plate covering a wide-FOV up to $\pm 40^\circ$ in the wavelength range from 640 to 1290 nm using the three-layer Au-SiO$_2$-Au nanostructure shown in Fig. 3a, which transforms an s-polarized incident wave from a propagation direction of $(\theta_i, \phi_i = 135^\circ)$ into a p-polarized reflected wave at a propagation direction of $(\theta_r, \phi_r = -45^\circ)$. During the design process, the effective polarizability tensors $\lambda_E$ and $\lambda_M$ of the anisotropic nanorod array metasurface were retrieved using the complex transmission and reflection coefficients for both polarizations at two angles of incidence (see Supplementary Information). The extracted effective surface polarizabilities were then used in the interference model to calculate the complex reflection coefficients $(r_{p\sigma}, r_{s\sigma})$ of the entire nanostructure over a wide angular range. In contrast to most of the previous observations and explanations of multilayer metalodielectric nanostructures in which magnetic resonances are identified, here it is found that the near-field interaction between the nanorod array and the continuous Au ground layer is weak enough to be neglected. Consequently, the interference model, which is more efficient in terms of the computation time, can be applied even though the dielectric layer thickness is on a subwavelength scale.

A powerful covariance matrix adaptation evolutionary strategy (CMA-ES) optimization technique was employed to identify the nanostructure dimensions that meet the challenging multi-objective half-wave plate design criteria, i.e. highly-efficient polarization conversion spanning a wide spectral and angular range. Predefined constraints on the allowable unit cell size, nanorod length and width, as well as the thickness of metal and dielectric layers were incorporated into the optimization algorithm to avoid generating structures that are impractical to fabricate. Additionally, experimentally measured dispersive optical properties for the constituent metal and dielectric materials were used to minimize discrepancies between the theoretically predicted and experimentally fabricated nanostructure response.

For each design candidate, the calculated reflection coefficients for both polarizations $(r_{p\sigma}, r_{s\sigma})$ in the targeted wavelength and angular range are compared with the user-input-defined target values to determine the Cost, which is expressed as:

$$Cost = \sum_{\lambda} \left( \frac{|r_{p\sigma}(\lambda) - r_{p\sigma}^{target}(\lambda)|^2 + |r_{s\sigma}(\lambda) - r_{s\sigma}^{target}(\lambda)|^2}{2} \right)$$
where $\lambda$ and $\theta_i$ denote the wavelength and incident angles included in the optimization. For this work, we selected wavelengths from 640 to 1290 nm in steps of 50 nm and angles from $0^\circ$ to $40^\circ$ in steps of $10^\circ$. The CMA-ES evolved solutions until it converged on a three-layer metal-dielectric nanostructure with a sufficiently low overall Cost value that achieved the desired half-wave plate optical properties. The optimized geometry of the structure that meets these design criteria is shown in Figs. 3a and 3b. The Au nanorods have a length of 210 nm and a width of 70 nm, which corresponds to an aspect ratio of 0.33. The periodicity in both the $x$- and $y$-directions is 252 nm, giving an inter-element gap of 42 nm in the $x$-direction, which provides strong electromagnetic coupling to the neighboring nanorods. The thickness values for the top Au nanorod array layer, the SiO$_2$ layer, and the bottom Au layer are 42 nm, 114 nm, and 100 nm, respectively, resulting in a structure that is only 256 nm thick.

The polarization conversion ratio (PCR) of the metasurface-based half-wave plate was calculated using the semi-analytical interference model, defined as:

$$\text{PCR}_{\text{hwp}} = \frac{|r_{pl}|^2}{|r_{pl}|^2 + |r_{sl}|^2}.$$

As shown by the theoretical curves plotted in Fig. 3d, the calculated $\text{PCR}_{\text{hwp}}$ is greater than 94% across the targeted broad wavelength and wide angular range, and remains above 90% over a wider band from...
640 to 1400 nm. Throughout this spectral and angular range, the reflection magnitude is greater than 95%, thereby achieving a much higher power efficiency than previous plasmonic metamaterial and metasurface-based designs.\(^4,\,22,\,31,\,33,\,34,\,46\). Even for angles of incidence as large as 50°, the reflection magnitude of the nanostructure is maintained above 94% with a PCR\(_{\text{hwp}}\) of greater than 83% (see Fig. S6). Notably, this example demonstrates that the bandwidth of the 2D array of strongly coupled nanorods is significantly wider than that of the freestanding pairs of nanorods (Fig. 2c–d).

For the optimized 2D nanorod array structure, at large incident angles, the in-band PCR\(_{\text{hwp}}\) is limited by: (1) the higher quality factors of two resonant peaks that correspond to the x- and y-directed LSPP dipolar modes of the coupled Au nanorods; and (2) the increase in phase retardation in the dielectric spacer. As a result, in the spectral range bracketed by the two modes, the reflection phase difference between the x- and y-directed electric field components exceeds 180° for incident angles greater than 40°. This causes the observed decrease in the PCR\(_{\text{hwp}}\) near the middle of the band between the resonant peaks, which restricts the FOV for >90% PCR\(_{\text{hwp}}\) to approximately ± 40°.

The state of polarization (SOP) traces of the incident and reflected light are presented in Fig. 3e at several angles of incidence and wavelengths within the band. Clearly defined cosine-shaped patterns can be identified, indicating that the reflected wave possesses a high degree of linear polarization (DoLP). The SOP patterns of the incident light have their maxima along the −90°/90° directions, while the SOP patterns of the reflected light have their maxima along the 0°/180° directions. The 90° rotation over the broad spectral and wide angular range confirms that the optimized plasmonic metasurface-based half-wave plate indeed transforms a linearly polarized incident wave into a reflected wave with a cross polarization.

**Experimental realization and characterization.** The optimized plasmonic metasurface-based half-wave plate was fabricated using conventional top-down lithography. Briefly, the process began by depositing the bottom continuous Au layer and the SiO\(_2\) layer on a Si handle wafer. The structure was completed by defining the topmost periodic nanorod array using electron-beam lithography followed by an Au lift-off process (see Methods for details). Field emission scanning electron microscope (FESEM) images of the fabricated nanostructure are shown in Fig. 3c. The measured dimensions of Au nanorod length, width, and minimum inter-element gap spacing are 210 ± 5 nm, 70 ± 3 nm, and 42 ± 4 nm. The lithographic process produces nanorods that have rounded corners, which results in effective electromagnetic gap spacing of 50 ± 2 nm. The PCR\(_{\text{hwp}}\) and reflection magnitude of the fabricated structure was characterized using a custom-built optical setup (see Fig. S8) that utilizes a supercontinuum source to illuminate the structure at incident angles of 4°, 20°, and 40° (see Methods). The strong peak in the power spectrum of the source at 1064 nm (the pump wavelength used to generate the supercontinuum) introduces significant measurement error; thus, data collected in the wavelength range between 1040 and 1080 nm are excluded from the plots.

The optical properties of the fabricated metasurface-based half-wave plate shown in Fig. 3d–e are in strong agreement with theoretical predictions. The measured PCR\(_{\text{hwp}}\) and reflection magnitude both remain above 92% over the targeted broad wavelength range from 640 to 1290 nm and wide-FOV from 0° to 40°. Even at a larger 50° angle of incidence, the PCR\(_{\text{hwp}}\) and reflection magnitude are still 86% and 87%, respectively (see Fig. S6). In comparison to the design, the long-wavelength cut-off for the 90% PCR\(_{\text{hwp}}\) bandwidth at a 4° incident angle is blue-shifted from 1400 to 1330 nm without a change in the short-wavelength cutoff. This small discrepancy is attributed to the wider inter-rod gap spacing in the fabricated structure compared to the optimized design dimensions. This is consistent with the trend found in the freestanding nanorod pair scattering analysis in Fig. 2c–d, which shows a blue shift in the x-directed LSPP dipolar resonance without affecting the y-directed dipolar resonance as the gap increases.

Polarization conversion is experimentally verified by the measured SOP patterns shown in Fig. 3e. The cosine-shaped patterns confirm the high DoLP of the reflected light. In addition, the angle between the maxima of the reflected and incident light patterns is 90° throughout the entire wavelength band and 40° FOV, indicating that the maximum light is reflected from the sample when the polarizers for the incident and reflected light are oriented orthogonally to each other. Compared to the current experimentally demonstrated plasmonic metasurface-based polarization-control devices, the nanorod array half-wave plate presented here achieves a high power efficiency over a wide spectral and angular range.

**Demonstration of a metasurface-based quarter-wave plate.** To show the versatility of the proposed platform and design approach, a metasurface-based quarter-wave plate was also optimized for the same spectral range of 640 to 1290 nm and wide-FOV from 0 to 40°. The three-layer structure shown in Fig. 4a transforms a circularly polarized incident wave from a direction (θ\(_iT\), φ\(_iT\) = 180°) into a linearly polarized reflected wave at a direction (θ\(_f\), φ\(_f\) = 0°), which provides an in-phase superposition of both the s- and p-polarizations. One unit cell of the optimized doubly periodic array is composed of 180 nm long and 70 nm wide Au nanorods that are centered within the 240 nm × 282 nm cell. This array structure possesses a weaker degree of anisotropy compared to the half-wave plate because of the larger nanorod aspect ratio of 0.5 and wider inter-element gap of 60 nm. As plotted in Fig. 4d, the simulated PCR\(_{\text{qwp}}\) is greater than 90% over a wider than targeted wavelength range from 620 to 1500 nm for incident angles up to 50° (see Fig. S7). The reflection magnitude is greater than 93% across the targeted spectral and angular range except for a narrow dip near 680 nm. The SOP traces presented in Fig. 4e show that the nanostructure transforms the incident wave with a circular SOP pattern into a reflected wave with a cosine pattern that has a maximum along the 45°/225° direction.

Figure 4c displays FESEM images of the nanofabricated quarter-wave plate. The measured dimensions of the Au nanorod length, width, and minimum inter-element gap spacing are 180 ± 6 nm, 90 ± 4 nm, and 60 ± 5 nm, which agree well with the design target. Similar to the quarter-wave plate, the rounded nanorod edges result in an effective gap of 68 ± 3 nm that is wider than the design target. During the characterization process, a commercial quarter-wave plate was used to generate circularly polarized incident light (see Fig. S8). As shown in Fig. 4d, the measured PCR\(_{\text{qwp}}\) is greater than 91% within the targeted wavelength range and angular range, with the reflection magnitude higher than 92%. The reduced PCR\(_{\text{qwp}}\) value in the long wavelength range can be attributed to the imperfect circular polarization of the incident wave above 1300 nm, which is outside of the operational band of the commercial quarter-wave plate. The measured SOP patterns are in strong agreement with the simulated predictions, indicating that the circularly polarized incident wave is effectively converted to a linearly polarized reflected wave.

**Discussion**

In conclusion, we have demonstrated a versatile approach to create highly efficient, wide-FOV plasmonic metasurface-based waveplates that control the polarization response of light over more than an octave bandwidth from the visible to the near-IR. The ultrathin reflective waveplates are realized by tailoring the spectral phase properties of a strongly coupled anisotropic nanorod array in conjunction with the interference of light between the array and the ground plane. A half-wave plate and a quarter-wave plate were designed and fabricated, achieving a PCR and reflection magnitude higher than 92% over more than an octave bandwidth from 640 to 1290 nm within a
wide field-of-view of $\pm 40^\circ$ for both devices. Beyond the two proof-of-concept waveplates, the general design approach presented in this work can be extended to nanostructured optical components that exhibit arbitrary polarization conversion properties, as well as other optical functionalities endowed by metasurfaces with engineered dispersion, over a broad wavelength and wide angular range.

**Methods**

**Numerical full-wave simulations.** The high frequency structure simulator (HFSS) finite element solver was used to perform all the full-wave simulations. For the scattering simulations of the single and coupled nanorod pair elements, the structures were placed in the center of an airbox whose outer edges were assigned a radiation boundary to prevent undesired reflections. The nanorod was oriented such that its long side coincides with the x-direction and its short side with the y-direction. Two linearly polarized plane waves, one x-polarized and the other y-polarized, were normally incident from the top surface of the nanorod elements. The scattered fields were evaluated at a distance of 3 mm below the bottom surface of the nanorod. The phase of the scattered fields was defined relative to that of the excitation when no nanorod elements are present. For the unit cell simulations of the three-layer metallodielectric waveplate and the metasurface on a SiO$_2$ half space, periodic boundary conditions were assigned to the lateral walls of the simulation domain to approximate an infinite array. Floquet ports were then added on the top and bottom faces of the simulation domain to obtain the reflection and transmission coefficients of a plane wave illuminating the nanostructure at an arbitrary angle of incidence.

**Device fabrication.** The three-layer metallodielectric structures were fabricated by first depositing a 10 nm Ti adhesion layer and the bottom 100 nm Au ground plane.
1. Kildishev, A. V., Boltasseva, A. & Shalaev, V. M. Planar photonics with incident light was provided by inserting a conventional broadband quarter-wave plate within the plane of incidence, based quarter-wave plate was characterized by confining the long axis of the nanorod perpendicular to the wave vector of the reflected light and detecting the transmitted fraction of the plasmonic metasurface-based half-wave plate, an s-polarized beam was produced by a polarization beam splitter and used as the incident light source. The polarization state of the reflected light was characterized by rotating a broadband analyzer in steps of 10° (Glan-Thompson Calcite Polarizer, Newport 10GT04) in the plane perpendicular to the vector of the reflected light and detecting the transmitted power with an Optical Spectrum Analyzer (Ando, OSA AQ 6315A). The metasurface based quarter-wave plate was characterized by confining the long axis of the nanorod 50% within the plane of incidence, i.e. the x-z plane in Fig. 4a. The circularly polarized incident light was produced by inserting a conventional broadband quarter-wave plate immediately after the polarization beam splitter and in front of the sample.

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Author contributions

Z.H.J. designed the metasurface-waveplate and developed the interference model. L.L. and S. fabricated the samples and took SEM images. Measurements were performed by D.M. together with L.L. and Z.H.J., D.H.W., Z.L. and T.S.M. supervised the project. All authors discussed the results and wrote the manuscript.

Additional information

Supplementary information accompanies this paper at http://www.nature.com/scientificreports
