Raman spectroscopy of graphene under ultrafast laser excitation

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The equilibrium optical phonons of graphene are well characterized in terms of anharmonicity and electron-phonon interactions; however, their non-equilibrium properties in the presence of hot charge carriers are still not fully explored. Here we study the Raman spectrum of graphene under ultrafast laser excitation with 3 ps pulses, which trade off between impulsive stimulation and spectral resolution. We localize energy into hot carriers, generating non-equilibrium temperatures in the ~1700–3100 K range, far exceeding that of the phonon bath, while simultaneously detecting the Raman response. The linewidths of both G and 2D peaks show an increase as function of the electronic temperature. We explain this as a result of the Dirac cones’ broadening and electron-phonon scattering in the highly excited transient regime, important for the emerging field of graphene-based photonics and optoelectronics.
The distribution of charge carriers has a pivotal role in determining fundamental features of condensed matter systems, such as mobility, electrical conductivity, spin-related effects, transport, and optical properties. Understanding how these properties can be affected and, ultimately, manipulated by external perturbations is important for technological applications in diverse areas, ranging from electronics to spintronics, optoelectronics and photonics.

The current picture of ultrafast light interaction with single-layer graphene (SLG) can be summarized as follows. Absorbed photons create optically excited electron-hole (e–h) pairs. The subsequent relaxation towards thermal equilibrium occurs in three steps. Ultrafast electron–electron (e–e) scattering generates a hot Fermi–Dirac distribution within the first tens fs. The distribution then relaxes due to scattering with optical phonons (ph; electron–phonon (e–ph) coupling), equilibrating within a few hundred fs. Finally, anharmonic decay into acoustic modes establishes thermodynamic equilibrium on the ps timescale.

Raman spectroscopy is one of the most used characterization techniques in carbon science and technology. The measurement of the Raman spectrum of graphene triggered a substantial effort to understand phonons, e–ph, magnetoph–ph, and e–e interactions in graphene, as well as the influence of the number and orientation of layers, electric or magnetic fields, strain, doping, disorder, quality and types of edges, and functional groups. The Raman spectra of SLG and few layer graphene (FLG) consist of two fundamentally different sets of peaks. Those, such as D, G, 2D, present also in SLG, and due to in-plane vibrations, and others, such as the shear (C) modes and the layer breathing modes due to relative motions of the planes themselves, either perpendicular or parallel to their normal. The G peak corresponds to in-plane vibrations at the high frequency of the 22 phonon at Γ. The D peak is due to the breathing modes of six-atom rings, and requires a defect for its activation. It originates from transverse optical (TO) phonons around the Brillouin Zone edge. Kohn Anomaly at K, it is active by double resonance (DR). The D peak is the D overtone and originates from a process where momentum conservation is fulfilled by two phonons with opposite wavevectors. It is always present since no defects are required for this process.

Raman spectroscopy is usually performed under continuous wave (CW) excitation, therefore probing samples in thermodynamic equilibrium. The fast e–e and e–ph non-radiative recombination channels establish equilibrium conditions between charge carriers and lattice, preventing the study of the vibrational response in presence of an hot e–h population. Using an average power comparable to CW illumination (a few mW), ultrafast optical excitation can provide large fluences (∼1–15 J m−2 at MHz repetition rates) over sufficiently short timescales (0.1–10 ps) to impulsively generate a strongly out-of-equilibrium distributions of hot e–h pairs. The potential implications of coupled e and ph dynamics for optoelectronics were discussed for nanoelectronic devices based on CW excitation. However, understanding the impact of transient photoinduced carrier temperatures on the colder SLG ph bath is important for mastering out of equilibrium e–ph scattering, critical for photonics applications driven by carrier relaxation, such as ultrafast lasers, detectors, and modulators. E.g, SLG can be used as a much
broader-band alternative to semiconductors saturable absorbers, for mode-locking and Q switching.

Here we characterize the SLG optical ph at high electronic temperature, \( T_e \), by performing Raman spectroscopy under pulsed excitation. We use a 3 ps pulse to achieve a trade-off between the narrow excitation bandwidth required for spectral resolution \( \frac{\Delta \nu}{\Delta t} \leq 10 \text{ cm}^{-1} \), being \( \nu [\text{Hz}] \) the laser frequency and \( c \) the speed of light, a condition met under CW excitation and a pulse duration, \( \delta t \), sufficiently short (\( \delta t \leq 10 \text{ ps} \), achieved using ultrafast laser sources) to generate an highly excited carrier distribution over the equilibrium ph population, being those two quantities Fourier conjugates (\( \delta \nu \leq 14.7 \text{ cm}^{-1} \text{ ps}^{-1} \)). This allows us to determine the dependence of both ph frequency and dephasing time on \( T_e \), which we explain by a broadening of the Dirac cones.

Results

Hot photoluminescence. Figure 1a plots a sequence of anti-Stokes (AS) Raman spectra of SLG following ultrafast excitation at 1.58 eV, as a function of excitation power \( P_e \). The broad background stems from hot photoluminescence (PL) due to the inhibition of a full non-radiative recombination under high excitation densities. This process, absent under CW excitation in pristine SLG, is due to ultrafast photogeneration of charge carriers in the conduction band, congesting the e-ph decay pathway, which becomes progressively less efficient with increasing fluence. This non-equilibrium PL recalls the gray body emission and can be in first approximation described by Planck’s law,

\[
R(\nu) = \frac{\nu^3}{2\pi^2 c^3 h^3} \frac{\hbar \nu^3}{2\pi^2 c^3} \left( e^{\frac{\hbar \nu}{kT}} - 1 \right)^{-1} \tag{1}
\]

where \( \eta \) is the emissivity, defined as the dimensionless ratio of the thermal radiation of the material to the radiation from an ideal black surface at the same temperature as given by the Stefan–Boltzmann law, \( \tau \), \( \tau \) is the emission time and \( \mathcal{R}(\nu) \) is the frequency dependent, dimensionless responsivity of our detection chain. Reported that, although Eq. 1 does not perfectly reproduce the entire gray body emission, the agreement on a \(-0.5 \text{ eV} \) energy window is sufficient to extract \( T_e \). By fitting the background of the Raman spectra with Eq. 1 (solid lines in Fig. 1a) we obtain \( T_e = 13.5 \text{ K} \). Figure 1b shows that \( T_e \) can reach up to 3100 K under our pulsed excitation conditions.

An upper estimate for the lattice temperature, \( T_1 \), can be derived assuming a full thermalization of the optical energy between vibrational and electronic degrees of freedom, i.e., evaluating the local equilibrium temperature, \( T_{\text{eq}} \), by a specific heat argument (see Methods). We get \( T_{\text{eq}}(P_{\text{max}}) \sim 680 \text{ K} \) at the maximum excitation power, \( P_{\text{max}} = 13.5 \text{ mW} \). This is well below the corresponding \( T_e \), indicating an out-of-equilibrium distribution of charge carriers. Thus, over our 3 ps observation timescale, \( T_1 \) is well below \( T_{\text{eq}} \).

Out of equilibrium Raman response. Figure 1c plots the AS and S G peaks, together with fits by Lorentzians (blue lines) convoluted with the laser bandwidth (\(-9.5 \text{ cm}^{-1} \)) and spectrometer resolution (\(-6 \text{ cm}^{-1} \)), which determine the instrumental response function, IRF (see Methods). The S data have a larger noise due to a more critical background subtraction, which also requires a wider accessible spectral range (see Methods). For this reason, we will focus on the AS spectral region, with an higher spectrometer resolution (1.2 cm\(^{-1}\)), Fig. 2. We obtain a full width at half maximum of the G peak, FWHM(G) \(~21 \text{ cm}^{-1} \), larger than the CW one (\(~12.7 \text{ cm}^{-1} \)). Similarly, we get FWHM(2D) \(~50–60 \text{ cm}^{-1} \) over our \( P_e \) range, instead of FWHM(2D) \(~29 \text{ cm}^{-1} \) as measured on the same sample under CW excitation. To understand the origin of such large FWHM(G) and FWHM(2D) in pulsed excitation, we first consider the excitation power dependence of the SLG Raman response in the 1.53−13.5 mW range (the lower bound is defined by the detection capability of our setup). This shows that the position of the G peak, Pos(G), is significantly blueshifted (as reported for graphite in ref\(^{33} \)), while the position of the 2D peak, Pos(2D), is close to that measured under CW excitation, and both FWHM(G) and FWHM(2D) increase with \( P_e \). Performing the same experiment on Si proves that the observed peaks broadening is not limited by our IRF (see Methods). Moreover, even the low resolution S data of the G band, collected in the range 1.8−7.0 mW (a selection is shown in Fig. 1c), display a broadening ((\( \pm 4 \times 10^{-3} \text{ cm}^{-1} \text{ K}^{-1} \)) and upshift ((\( \pm 1.8 \times 10^{-3} \text{ cm}^{-1} \text{ K}^{-1} \)), compatible with that of the high-resolution AS measurements (Fig. 3d, e) (\( 2.4 \pm 0.5 \times 10^{-3} \text{ cm}^{-1} \text{ K}^{-1} \) and \( 3.2 \pm 0.2 \times 10^{-3} \text{ cm}^{-1} \text{ K}^{-1} \)).

We note that phonons temperature estimates based on the AS/ S intensity ratio\(^{37,38} \) are not possible in our case due to two concurring effects. First, SLG’s resonant response to any optical wavelength gives a non trivial wavelength dependent Raman excitation profile, which modifies the Raman intensities with respect to the non-resonant case. Consequently, the AS/S ratio is no longer straightforwardly related to the thermal occupation. Second, in SLG a S ph may be subsequently annihilated by a correlated AS event. This may result into an extra AS pumping which does not allow to relate AS/S ratio and ph temperature via the thermal occupation factor\(^{40} \). Accordingly, the AS/S ratio approaching one at the largest excitation power in Fig. 1c (black circles) does not necessarily imply a large increase of the G phonon temperature.
**Fig. 3** Comparison between theory and experiments. **a** Pos(2D), **b** FWHM(2D), **d** Pos(G), **e** FWHM(G) as a function of $T_e$ for ps-excited Raman spectra. Error bars represent the 95% confidence level in the best fitting procedure. Solid diamonds in **a,b,d,e** represent the corresponding CW measurements. FWHM(2D) are used to determine the e-e contribution ($\gamma_{ee}$) to the Dirac cone broadening, shown in **c** (blue lines). Pos(G) and FWHM(G) are compared with theoretical predictions accounting for e-ph interaction in presence of electronic broadening (an additional RT anharmonic damping $\sim 2 \text{ cm}^{-1}$) is included in the calculated FWHM(G)). Black lines are the theoretical predictions for $\gamma_{ee} = 0$ eV, while blue lines take into account an electronic band broadening linearly proportional to $T_e$ ($\gamma_{ee} = \alpha \delta T_e$). From the fit of $\gamma_{ee}$ in **c**, we get $\alpha = 0.51 \text{ cm}^{-1} \text{ K}^{-1}$, corresponding to 95% confidence boundaries, are also shown (thin light blue lines).

**Discussion**

Figure 3 plots Pos(2D), FWHM(2D), Pos(G), FWHM(G) as a function of $T_e$ estimated from the hot-PL. A comparison with CW measurements (633 nm) at room temperature (RT) is also shown (blue diamonds). Under thermodynamic equilibrium, the temperature dependence of the Raman spectrum of SLG is dominated by anharmonicity, which is responsible for mode softening, leading to a redshift of the Raman peaks. This differs from our experiments (Fig. 4a–d), in which Pos(G) has an opposite trend (blue shift), and Pos(G) is nearly $T_e$ independent, in agreement with density functional perturbation theory (DFPT) calculations, giving a variation of the 2D peak $\Delta$Pos(2D) $\sim 5 \text{ cm}^{-1}$ in the range $T_e = 300–3000 \text{ K}$ (see Methods). This indicates the lack of significant anharmonic effects and suggests a dominant role of e-ph interaction on FWHM(G) and Pos(G), in the presence of a cold phonon bath at constant $T_1$ decoupled from the (large) $T_e$.

To derive the temperature dependence of such parameters, we first compute the phonon self-energy $\Pi(q = 0, \omega_0^G)$, as for refs. 22, 43, 44,

$$\Pi(q = 0, \omega_0^G, T_e) = \xi \int_0^{\omega_0^G} \frac{d\omega}{\omega} \int_0^{\infty} \frac{d\omega'}{\omega'} \sum_{s,s'} f_s(z - \omega) - f_s(z' - \omega') \left[ \frac{\omega_0^G}{z - z'} + \frac{\omega_0^G}{\omega} + i\delta \right]$$

(2)

Here $\xi = \tilde{g}^2/(2h\gamma_{el}^a)$, $\gamma_{el}^a = 4.43 \times 10^{-3}$ is a dimensionless constant, $\omega_0^G$ is the Fermi velocity, $\omega$ is the upper cutoff of the linear dispersion $\varepsilon = \omega_0^G k$, $\omega_0^G$ is the carbon atom mass, $\omega_0^G = 0.196 eV$ the bare phonon energy, $\delta$ is a positive arbitrary small number ($\lesssim 4 \text{ meV}$), $\omega \sim 12.3 \text{ eV}$ is proportional to the e-ph coupling in the SLG, $z, z'$ are the energy integration variables and $f_s(z - \omega)$ is the Fermi–Dirac distribution with $E_0$ the Fermi energy. Although our samples are doped, $E_0$ significantly decreases as a function of $T_e$. Hence, we assume $E_0 = 0$ in the following calculations. The two indexes $s,s' = \pm 1$ denote the e and h branches, and $M_s(z, \omega)$ is the corresponding spectral function, which describes the electronic dispersion.

The self-energy expressed by Eq. 2 renormalizes the phonon Green’s function according to the Dyson’s equation: 46

$$D(\omega) = \frac{2\omega_0^G}{(\omega_0^G + i\delta)^2 - (\omega_0^G)^2}$$

(3)

so that $\Delta \text{Pos}(G)$ and FWHM(G) can be written as:

$$\Delta \text{Pos}(G) = \frac{1}{\hbar \omega} \text{Re} [\Pi(0, \omega_0^G, T_e) - \Pi(0, \omega_0^G, T_e = 0)]$$

FWHM(G) = $-$ $\frac{2}{\hbar \omega} \text{Im} \Pi(0, \omega_0^G, T_e)$

(4)

where $h$ is the Planck constant, FWHM(G) can be further simplified since the evaluation of $\text{Im} \Pi(0, \omega_0^G, T_e)$ leads to $\omega(\omega-z' - \omega_0^G)$ in Eq. 2, so that we get:

$$\text{FWHM}(G) = \frac{\pi\xi}{3\hbar} \int_0^{\omega_0^G} \frac{d\omega}{\omega} \int_0^{\infty} \frac{d\omega'}{\omega'} \sum_{s,s'} f_s(z) - f_s(z' - \omega_0^G)$$

(5)

In the limit of vanishing broadening of the quasiparticle state, the SLG gapless linear dispersion is represented by the following spectral function: 46

$$M_s(z, \omega) = \delta(z + se), \quad s = \pm 1,$$

(6)

This rules the energy conservation in Eq. 5 and allows only transitions between h and e states with energy difference $2e = \omega_0^G$. Thus, we get: 22, 43, 44

$$\text{FWHM}(G) = \text{FWHM}(G)^0 [f_h(-\omega_0^G/2) - f_e(\omega_0^G/2)]$$

(7)

where FWHM(G)$^0 = \frac{2\omega_0^G}{(\omega_0^G)^2} \sim 11 \text{ cm}^{-1}$ 10. This value, with the additional $\sim 2 \text{ cm}^{-1}$ contribution arising from anharmonic effects, is in agreement with the CW measurements at $T_e = T_{eq} = 300 \text{ K}$ (see diamond in Fig. 3e), corresponding to fluences $\lesssim 1 \text{ J} \text{ m}^{-2}$. Eq. 7 also shows that, as $T_e$ increases, the conduction band becomes increasingly populated, making the phonon decay channel related to e-h formation progressively less efficient and leading to an increase of the ph decay time (Fig. 4b). This leads to a decrease of FWHM(G) for increasing $T_e$ (black solid line in Fig. 3e), in contrast with the experimentally observed increase (blue circles in Fig. 3e).

A more realistic description may be obtained by accounting for the effect of $T_e$ on the energy broadening ($\gamma_{ee}$) of the linear dispersion $M_s(x,e)$, along with the smearing of the Fermi function.
\[ \gamma_s(z, T_e) \] can be expressed, to a first approximation, as the sum of three terms:\[8\]
\[ \gamma_s(z, T_e) = \gamma_{ee}(T_e) + \gamma_{ep}(z) + \gamma_{df}(z) \]  
where \( \gamma_{ee} \), \( \gamma_{ep} \), and \( \gamma_{df} \) are the e–e, e–ph and defect contributions to \( \gamma_s \). The only term that significantly depends on \( T_e \) is \( \gamma_{ee} \), while the others depend on the energy \( \epsilon_z \) in the spectral function of Eq.6:

\[ \Delta \text{FWHM}(2D) = 4 \sqrt{2} / 3 - \frac{1}{2} \nabla S(2D) / \nabla S(h \nu_{\text{las}}) \gamma_{ee} \]  

where \( \nabla S(2D) / \nabla S(h \nu_{\text{las}}) / 2 = \frac{1}{\pi} \mu_{ph} / \mu_{ee} \sim 100 \text{cm}^{-1} \text{eV}^{-1} \), i.e., the ratio between the ph and Fermi velocity, defined as the slope of the phononic (electronic) dispersion at the ph (e) momentum corresponding to a given excitation laser energy \( h \nu_{\text{las}} \). Since the DR process responsible for the 2D peak involves the creation of e–h pairs at energy \( \epsilon = h \nu_{\text{las}} / 2 \), the change of FWHM(2D) allows us to estimate the variation of \( \gamma_s \) at \( z = h \nu_{\text{las}} / 2 \approx 0.8 \text{eV} \). Then, \( \gamma_{ep} \) and \( \gamma_{df} \) both proportional to \( z \) (\( \gamma_{ep}, \gamma_{df} \propto z \)), will give an additional constant contribution to FWHM(2D), but not to its variation with \( T_e \). Our data support the predicted linear increase of \( \gamma_{ee} \) with \( T_e \), with a dimensionless experimental slope \( \alpha_s \approx 0.73 \), Fig. 3c.

In order to compute FWHM(G) from Eq. 2, we note that the terms \( \gamma_{ep} \) and \( \gamma_{df} \) are negligible at the relevant low energy \( z = h \nu_{G} / 2 \sim 0.1 \text{eV} \ll h \nu_{\text{las}} / 2 \). Hence \( \gamma_s(z, T_e) \approx \gamma_{ee}(T_e) \).

The Dirac cone broadening can now be introduced by accounting for \( \gamma_e \) in the spectral function of Eq. 6:

\[ M_s(z) = \frac{1}{\pi} \frac{\gamma_e}{\left(z + \epsilon_0\right)^s + \left(\epsilon_0/2\right)^s}, \quad s = \pm 1 \]  

accordingly, all the processes where the energy difference \( |s\epsilon(k) - s\epsilon(k')| + h \omega_d \) is less than \( 2\epsilon_e \) (which guarantees the overlap between the spectral functions of the quasiparticles) will now contribute in Eq. 2. Amongst them, those transitions within the same (valence or conduction) band, as shown in Fig. 4d.

The broadened interband contributions still follow, approximately, Eq. 7 (Fig. 4e). However, the Dirac cone broadening gives additional channels for G phonon annihilation by carrier excitation. In particular, intra-band transitions within the Dirac cone are now progressively enabled for increasing \( T_e \), as sketched in Fig. 4d. In Fig. 4e the corresponding contributions to FWHM(G) are shown. Calculations in the weak-coupling limit\[51\] suggest that \( \gamma_s(T_e) \) should be suppressed as \( z \to 0 \), due to phase–space restriction of the Dirac cone dispersion. Our results, however, indicate that this effect should appear at an energy scale smaller than \( \hbar \omega_{G}/2 \), as the theory captures the main experimental trends, just based on a \( z \)-independent \( \gamma_e(T_e) \).

Critically, the G peak broadening has a different origin from the equilibrium case\[53\]. The absence of anharmonicity would imply a FWHM(G) decrease with temperature due to the e–ph mechanism. However, the Dirac cone broadening reverses this trend into a linewidth broadening above \( T_e = 1000 \text{K} \) producing, in turn, a dephasing time reduction, corresponding to the experimentally observed FWHM(G) increase. The blue shift of the G peak with temperature is captured by the standard e–ph interaction, beyond possible calibration accuracy. Importantly, the Dirac cone broadening does not significantly affect \( \text{Pos}(G) \).

In conclusion, we measured the Raman spectrum of SLG with impulsive excitation, in the presence of a distribution of hot charge carriers. Our excitation bandwidth enables us to combine frequency resolution, required to observe the Raman spectra, with short pulse duration, needed to create a significant population of hot carriers. We show that, under these strongly non-equilibrium conditions, the Raman spectrum of graphene cannot be understood based on the standard low fluence picture, and we provide the experimental demonstration of a broadening of the electronic linear dispersion induced by the highly excited carriers. Our results shed light on a peculiar regime of non-equilibrium Raman response, whereby the e–ph interaction is enhanced. This has implications for the understanding of transient charge carrier mobility under photoexcitation, important to study SLG-based optoelectronic and photonic devices\[27,28\], such as broadband light emitters\[29\], transistors and optical gain media\[34\].
Methods

Sample preparation and CW raman characterization. SLG is grown on a 35 μm Cu foil, following the process described in Refs.\textsuperscript{55,56}. The substrate is heated to 1000 °C and annealed in hydrogen (H\textsubscript{2}, 20 sccm) for 30 min. Then, 5 sccm of methane (CH\textsubscript{4}) is fed into the chamber for the following 30 min so that the growth can take place.\textsuperscript{55,56} The sample is then cooled back to RT in vacuum (<1 mTorr) and unloaded from the chamber. The sample is characterized by CW Raman spectroscopy using a Renishaw inVia Spectrometer equipped with a 100× objective. The Raman spectrum measured at 514 nm is shown in Fig. 5 (red curve). This is obtained by removing the non-flat background Cu PL\textsuperscript{57,58}. The absence of a significant D peak is another indication of the high quality of the SLG, which is in contrast with the well-defined 2D peak related to the 2D mode of the SLG.\textsuperscript{57,58} The 2D peak is a single sharp Lorentzian with FWHM(Si) = 23 cm\textsuperscript{-1}, a signature of SLG\textsuperscript{52}. Pos(G) is ~1587 cm\textsuperscript{-1}, with FWHM(G) ~14 cm\textsuperscript{-1}. Pos(2D) is ~2705 cm\textsuperscript{-1}, while the 2D to G peak area ratio is ~4.3. SLG is then transferred on glass by a wet method\textsuperscript{59}. Poly-methyl methacrylate (PMMA) is spin coated on the substrate, which is then placed in a solution of ammonium persulfate (APS) and deionized water. Cu is etched\textsuperscript{55,56}, the PMMA membrane with attached SLG is then moved to a beaker with deionized water to remove APS residuals. The membrane is subsequently lifted with the target substrate. After drying, PMMA is removed in acetone leaving SLG on glass.

The SLG quality is also monitored after transfer. The Raman spectrum of the substrate shows features in the D and G peak range, convoluted with the spectrum of SLG on glass (blue curve in Fig. 5). A point-to-point subtraction is needed to reveal the SLG features. After transfer, the D peak is still negligible, demonstrating that no significant additional defects are induced by the transfer process. The fitted Raman parameters indicate p-doping ~250 meV\textsuperscript{50,60}.

Before and after the pulsed laser experiments, CW CS measurements are performed at RT using a micro-Raman setup (LabRAM Infinity). A different energy and momentum of the D phonon is involved, for a given excitation wavelength, in the S or AS processes, due to the phonon dispersion in the DR regime (dashed black line). Error bars represent the 95\% confidence level of the best fit of the Si (a) and SLG (G) band peaks by ~130 cm\textsuperscript{-1}, resulting in PL suppression. The background subtraction requires in this case a wider spectral range, at the expenses of spectrometer resolution which is definitely smaller than for AS. For this reason we mostly focus on the AS features.

To verify that the observed peaks broadening is not limited by our IRF, we perform the same experiment on a Si substrate (Fig. 6a). For this we retrieve, after the deconvolution of the IRF, the same Raman linewidth measured in the CW excitation regime (Fig. 6a). The FWHM of the Si optical phonon is independent of \( P_L \), in contrast with the well-defined dependence on \( P_L \) observed in SLG, Fig. 6b.

Estimate of \( T_{eq} \). Photoc excitation of Si induces an excess of energy in the form of heat per unit area, \( Q \), that can be expressed as:

\[
Q = \frac{P_L}{\pi R^2} A \frac{a_0}{b_0},
\]

where \( A = 2.3\% \) is the SLG absorption, approximated to the undoped case\textsuperscript{61}, \( W \approx 2.8\mu m \) is the waist of focused beam and \( RR = 40 \mu m \) is the repetition rate of the excitation laser. The induced \( T_{eq} \) can be derived based on two assumptions: (i) in our ps timescale the energy absorbed in the focal region does not diffuse laterally, (ii) the energy is equally distributed on each degree of freedom (electrons, optical and acoustic PhD). Then, \( Q \) can be described as:

\[
Q = \int_{RT} C(T) dT
\]

where \( C(T) \) is the SLG T-dependent specific heat. In the 300–700 K range, \( C(T) \) can be described as\textsuperscript{62}:

\[
C(T) = aT + b, \quad a = 1.35 \times 10^{-9} \text{ J K}^{-2} \text{ m}^{-2}, \quad b = 1.35 \times 10^{-4} \text{ J} \text{ K}^{-1} \text{ m}^{-2}.
\]

Therefore, considering Eqs. 11, 12, for \( P_L = max = 13.5 \text{ mW} \), we get \( T_{eq} \sim 680K \), well below the corresponding \( T_c \), indicating an equilibrium condition \( T_{eq} < T_c \). Any contributions from the substrate and taking into account the heat profile would contribute in reducing even further \( T_c \) estimation.

Estimate of Pos(2D) as a function of \( T_c \). We perform calculations within the local density approximation in DFPT\textsuperscript{69,70}. We use the experimental lattice parameter 2.46 A\textsubscript{15} and plane waves (45 Ry cutoff), within a norm-conserving pseudopotential approach\textsuperscript{71}. The electronic levels are occupied with a Fermi–Dirac distribution, and we sample a Brillouin Zone with a 160 × 160 × 1 mesh. This does not take into account anharmonic effects, assuming \( T_c = 300K \). Figure 7 shows a weak \( \Delta \text{Pos}(2D) \sim 5 \text{ cm}^{-1} \) in the range \( T_c = 300–3000 K \). In equilibrium, \( T_c = T_{eq} \) would induce a non-negligible anharmonicity\textsuperscript{72}, which would lead to a Pos(2D) softening: \( \Delta \text{Pos}(2D)/a_{2D} \sim -0.05 \text{ cm}^{-1} \). The weak dependence \( \Delta \text{Pos}(2D)(P_L) \) (blue circles in Fig. 7) rules out a dominant anharmonicity contribution and, consequently, \( T_{eq} = T_c \). The minor disagreement with DFPT suggests a \( T_c \) slightly larger than RT, but definitely smaller than \( T_{eq} \).

Data availability. All relevant data are available from the authors.
Fig. 7 Temperature dependence of $\Delta$Psd(2D). Pos(2D), relative to the RT CW measurement, as a function of $T_e$. Black line: DFPT; blue circles: experimental data with pulsed excitation. Red line: $T$-dependent CW measurement in thermal equilibrium ($T_e = T = T_{eq}$) from ref 72. The error bars represent the 95% of confidence level as in Fig. 3

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References

1. Bonaccorso, F., Sun, Z., Hasan, T. & Ferrari, A. C. Graphene photonics and optoelectronics. Nat. Photonics 4, 611–622 (2010).
2. Ferrari, A. C. et al. Science and technology roadmap for graphene, related two-dimensional crystals, and hybrid systems. Nanoscale 7, 4598–4810 (2015).
3. Koppens, F. H. L. et al. Photodetectors based on graphene, other two-dimensional materials and hybrid systems. Nat. Nanotechnol. 9, 780–793 (2014).
4. Brida, D. et al. Ultrafast collinear scattering and carrier multiplication in graphene. Nat. Commun. 4, 1987 (2013).
5. Tomadin, A., Brida, D., Cerullo, G., Ferrari, A. C. & Polini, M. Nonequilibrium dynamics of photoexcited electrons in graphene: Collinear scattering, auger processes, and the impact of screening. Phys. Rev. B 88, 035430 (2013).
6. Lazzeri, M., Piscanec, S., Mauri, F., Ferrari, A. C. & Robertson, J. Electron transport and hot phonons in carbon nanotubes. Phys. Rev. Lett. 95, 236802 (2005).
7. Butscher, S., Milde, F., Hirschtrut, M., Mali, E. & Knorr, A. Hot electron relaxation and phonon dynamics in graphene. Appl. Phys. Lett. 91, 203103 (2007).
8. Lui, C. H., Mak, K. F. S., Shan, J. & Heinz, T. F. Ultrafast photoluminescence from graphene. Phys. Rev. Lett. 105, 127401 (2010).
9. Wu, S. et al. Hot phonon dynamics in graphene. Nano Lett. 12, 5495–5499 (2012).
10. Bonini, N., Lazzeri, M., Marzari, N. & Mauri, F. Phonon anharmonicities in graphene and graphite. Phys. Rev. Lett. 99, 176802 (2007).
11. Ferrari, A. C. & Robertson, J. C. Raman spectroscopy in carbons: from nanotubes to diamond, theme issue. Philos. Trans. R. Soc. Lond. A 362, 2267–2265 (2004).
12. Ferrari, A. C. et al. Raman spectrum of graphene and graphite layers. Phys. Rev. Lett. 97, 187401 (2006).
13. Ferrari, A. C. & Basko, D. M. Raman spectroscopy as a versatile tool for studying the properties of graphene. Nat. Nanotechnol. 8, 235–246 (2013).
14. Malard, L., Pimenta, M., Dresselhaus, G. & Dresselhaus, M. Raman spectroscopy in graphene. Phys. Rep. 473, 51–87 (2009).
15. Froehlicher, G. & Bercaud, S. Raman spectroscopy of electrochemically gated graphene transistors: Geometrical capacitance, electron-phonon, electron-electron, and electron-defect scattering. Phys. Rev. B 91, 205413 (2015).
16. Tan, P. H. et al. The shear mode of multilayer graphene. Nat. Mater. 11, 294–300 (2012).
17. Sato, K. et al. Raman spectra of out-of-plane phonons in bilayer graphene. Phys. Rev. B 84, 035419 (2011).
18. Liu, C. H. et al. Observation of layer-breathing mode vibrations in few-layer graphene through combination raman scattering. Nano Lett. 12, 5359–5364 (2012).
19. Tuinstra, F. & Koenig, J. L. Raman spectrum of graphite. J. Chem. Phys. 53, 1126–1130 (1970).
20. Thomsen, C. & Reich, S. Double resonant raman scattering in graphite. Phys. Rev. Lett. 85, 5214–5217 (2000).
21. Ferrari, A. C. & Robertson, J. Interpretation of raman spectra of disordered and amorphous carbon. Phys. Rev. B 61, 14095–14107 (2000).
55. Bae, S. et al. Roll-to-roll production of 30-inch graphene films for transparent electrodes. Nat. Nanotech. 5, 574–578 (2010).
56. Li, X. et al. Large-area synthesis of high-quality and uniform graphene films on copper foils. Science 324, 1312–1314 (2009).
57. Lagatsky, A. A. et al. 2m solid-state laser mode-locked by single-layer graphene. Appl. Phys. Lett. 102, 013113 (2013).
58. Cançado, L. G. et al. Quantifying defects in graphene via raman spectroscopy at different excitation energies. Nano Lett. 11, 3190–3196 (2011).
59. Bonaccorso, F. et al. Production and processing of graphene and 2d crystals. Mater. Today 15, 564–589 (2012).
60. Das, A. et al. Monitoring dopants by raman scattering in an electrochemically top-gated graphene transistor. Nat. Nanotech. 3, 210–215 (2008).
61. Baranov, A. V., Bekhterev, A. N., Bobovich, Y. S. & Petrov, V. I. Interpretation of certain characteristics in raman spectra of graphite and glassy carbon. Opt. Spectrosc. 62, 612–616 (1987).
62. Thomsen, C. & Reich, S. Double resonant raman scattering in graphite. Phys. Rev. Lett. 85, 5214–5217 (2000).
63. Tan, P. et al. Probing the phonon dispersion relations of graphite from the double-resonance process of Stokes and anti-Stokes raman scatterings in multiwalled carbon nanotubes. Phys. Rev. B 66, 245410 (2002).
64. Cançado, L. G. et al. Stokes and anti-Stokes double resonance raman scattering in two-dimensional graphite. Phys. Rev. B 66, 035415 (2002).
65. Marangoni, M. et al. Narrow-bandwidth picosecond pulses by spectral compression of femtosecond pulses in a second-order nonlinear crystal. Opt. Express 15, 8884–8891 (2007).
66. Liu, W.-T. et al. Nonlinear broadband photoluminescence of graphene induced by femtosecond laser irradiation. Phys. Rev. B 82, 081408 (2010).
67. Nair, R. R. et al. Fine structure constant defines visual transparency of graphene. Science 320, 1308–1308 (2008).
68. Pop, E., Varshney, V. & Roy, A. K. Thermal properties of graphene: Fundamentals and applications. MRS Bull. 37, 1273–1281 (2012).
69. de Gironcoli, S. Lattice dynamics of metals from density-functional perturbation theory. Phys. Rev. B 51, 6773–6776 (1995).
70. Giannozzi, P. et al. Quantum espresso: a modular and open-source software project for quantum simulations of materials. J. Phys. Condens. Matter 21, 395502 (2009).
71. Wang, Y., Panzik, J. E., Kiefer, B. & Lee, K. K. M. Crystal structure of graphite under room-temperature compression and decompression. Sci. Rep. 2, 520 (2012).
72. Net, C. et al. High-yield fabrication of nm-size gaps in monolayer cvd graphene. Nanoscale 6, 7249–7254 (2014).

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Author contributions

T.S. led the research project, conceived with G.C., F.M. and A.C.F.; C.Fe., A.V., and T.S. designed and built the pulsed Raman setup; C.Fe. and A.V. performed the out of equilibirum Raman experiments, with contribution from M.M.; C.Fa., P.P., D.D.F., U.S., A.K. O., and D.Y. performed the equilibrium CW Raman experiment; L.B. and F.M. developed the modeling and carried out the numerical simulations, with contributions from A. V.; D.D.F., U.S., A.K.O., and D.Y. prepared and characterized the samples; C.Fe., A.V., L. B., G.C., F.M., A.C.F., and T.S. interpreted the data and the simulations and wrote the manuscript.

Additional information

Competing interests: The authors declare no competing financial interests.

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