Discriminating Supersymmetry and Black Holes at the CERN Large Hadron Collider

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I. INTRODUCTION

At CERN’s Large Hadron Collider (LHC) [1] protons will soon collide at an astonishing $800 \times 10^6$ times per second to provide experimental evidence for the Higgs [2,3], supersymmetry (SU5) [4–6] or extra dimensions [7–10]. SUSY is widely considered to be one of the best candidates for physics beyond the standard model (SM). It provides an explanation for the Higgs mass problem, a candidate for cold dark matter, and unification of low energy gauge couplings by introducing superpartners to SM fields (see Ref. [11] and references therein). An alternative to SUSY is given by phenomenological extra-dimensional models such as large extra dimensions (LEDs) [8], warped braneworlds [9] or universal extra dimensions [10]. Scenarios with LEDs are specially appealing. In these models, gravity becomes strong at the TeV scale, where radiative stability is achieved. The fundamental scale of gravity, $M_\ast \sim 1 \text{ TeV}$, is related to the observed Planck scale, $M_{Pl}$, by the relation $M_{Pl}^2 \sim V_n M_\ast^{n+2}$, where $V_n$ is the volume of the extra $n$-dimensional space and $M_\ast$ is defined as in Ref. [12]. One of the most astounding consequences of the existence of extra dimensions would be the production of subatomic black holes (BHs) in particle colliders [13,14] and cosmic ray showers [15]. (For reviews, see Refs. [12,16].)

The ATLAS [17] and CMS [18] experiments at the LHC are entrusted with the task of studying events with large transverse momentum ($P_T$), a signature common to both SUSY and extra dimensions. While we wait for these experiments to start collecting data, it is worthwhile to look into means of distinguishing SUSY and extra-dimensional models [19]. Comparisons of SUSY and universal extra dimensions/little Higgs models in colliders have been investigated by various authors [20]. Discrimination of SUSY and BH events by means of dilepton events was recently discussed by the authors in Ref. [21]. In this paper, we revisit that analysis and extend it to include event-shape variables, missing transverse momentum $\not{P}_T$ and visible energy. BH and SUSY events are simulated with the BH generator CATFISH [22] and the high-energy event generator PYTHIA [23], respectively. SUSY masses are set with ISAJET [24]. The analysis below will show that SUSY and BH events can be clearly distinguished at the LHC. BH events tend to be more spherical than SUSY events because of the isotropic nature of BH decay. Thus event-shape variables, such as sphericity, provide good discriminators. On the contrary, visible energy and $\not{P}_T$ are less effective discriminators because of the presence of invisible channels in both SUSY and BH models, which make the amount of $\not{P}_T$ comparable in the two scenarios. The dilepton invariant mass is also an excellent discriminator; the SUSY invariant mass shows a sharp cutoff at $\sim 100$ GeV, which is absent in the BH model because most of the dileptons originate from uncorrelated events.

The remainder of this paper is organized as follows. In Sec. II and III we briefly review the fundamentals of SUSY and TeV BHs which are needed for our analysis, respectively. Simulations are described in Sec. IV. The analysis of visible/missing momentum and event-shape variables is presented in Sec. VA, and the discrimination of SUSY and BH using dileptons is discussed in Sec. VB. Conclusions are presented in Sec. VI.
TABLE I. Parameters for the five mSUGRA points discussed in the text. The scalar mass and the gaugino mass are given in GeV.

| LHC point | $m_0$ | $m_{1/2}$ | $A_0$ | $\tan \beta$ | $\mu$ |
|-----------|-------|-----------|-------|-------------|-------|
| A         | 100   | 300       | 300   | 2.1         | +     |
| B         | 400   | 400       | 0     | 2           | +     |
| C         | 400   | 400       | 0     | 10          | +     |
| D         | 200   | 100       | 0     | 2           | -     |
| E         | 800   | 200       | 0     | 10          | +     |

(i) $m_0$, the common scalar mass at $M_{\text{GUT}}$;
(ii) $m_{1/2}$, the common gaugino mass at $M_{\text{GUT}}$;
(iii) $A_0$, the common trilinear coupling at $M_{\text{GUT}}$;
(iv) $\tan \beta$, the ratio of the vacuum expectation values of the two Higgs fields;
(v) $\mu$, the sign of the Higgsino mass parameter.

mSUGRA parameters for five typical LHC points are given in Table I [25]. Neutralino ($\tilde{\chi}_0^0$), gluino ($\tilde{g}$) and squark ($\tilde{q}$) masses are determined by $m_0$ and $m_{1/2}$ as $\tilde{\chi}_0^0 \sim m_{1/2}/2$, $\tilde{\chi}_2^0 \sim \tilde{\chi}_1^0 \sim m_{1/2}$, $\tilde{g} \sim 3m_{1/2}$ and $m(\tilde{q}) \sim (m_0^2 + 6m_{1/2}^2)^{1/2}$ [26].

Visible energy, missing transverse momentum and sphericity for the five LHC points of Table I are shown in Fig. 1, where all SUSY processes except SM Higgs production have been implemented. Sparticle production at point D (open circles) is higher as squarks and gluinos are lighter. This point is usually taken as the comparison point between the LHC and other experiments, e.g. Tevatron [27] and NLC [28]. For the purposes of our analysis, the difference between the five points is not significant and any of them can be chosen as SUSY benchmark. In the following, we will consider point A. This is justified by the fact that point A allows for SUSY Higgs production [29]. Since BHs may evaporate into Higgs (see Sec. III below), a meaningful comparison of SUSY and BH events requires the presence of the Higgs channel in both models. Moreover, distinguishability of SUSY and BH events must be assessed by minimizing the differences between the two models. Since BH events are characterized by up to several TeV of missing transverse momentum, SUSY points with large $p_T$, such as point A, must be considered.

A symmetry of the MSSM is $R$-parity [4]:

$$P_R = (-1)^{3B+L+s},$$

where $B (L)$ is the baryon (lepton) number and $s$ is the particle spin. All SM particles have $P_R = +1$ whereas their superpartners have $P_R = -1$. $R$-parity implies that SUSY particles are always pair produced from SM particles. If $R$-parity is conserved, the endpoint of a SUSY process at the LHC is a state with SM particles and two lightest stable SUSY particles (LSPs), which are generally neutralinos. Being colorless and chargeless, the LSPs escape the detector and are the source of missing transverse momentum, a leading signature of SUSY events. If $R$-parity is not conserved, the missing transverse energy is reduced by the LSP decay. In the following, we will assume that $R$-parity is conserved, in agreement with the MSSM (mSUGRA) scenario.

We end this section with a list of dominant SUSY interactions at LHC point A and the definition of invariant mass. This is important for the following analysis because it enables us to select processes that could serve as potential discriminators. The third decay chain in Fig. 2 is specially interesting because it allows the separation of isolated leptons from the hadronic background [30]. The invariant mass is defined as

$$M_{12} = \sqrt{(E_1 + E_2)^2 - (p_1 + p_2)^2} = \sqrt{2p_1 \cdot p_2 (1 - \cos \theta)},$$

where $\theta$ is the angle between the two particles. The method

FIG. 1 (color online). Comparison of visible energy (left), missing transverse momentum $p_T$ (middle) and sphericity (right) for 10,000 events for the five LHC points of Table I (A: filled circles, B: filled squares, C: filled triangles, D: open circles and E: open squares).
of constructing invariant masses from SUSY decay chains has been traditionally used to calculate sparticle masses [29]. In Sec. V B we will use the invariant mass of isolated dileptons with large $P_T$ as a potential SUSY/BH discriminator. (For a review on lepton production at colliders, see Ref. [31].) In the rest frame of the second lightest neutralino, the dilepton invariant mass is

$$M_{ll} = \left[ M_{\tilde{\chi}^0_2}^2 + M_{\tilde{\chi}^0_1}^2 - 2M_{\tilde{\chi}^0_2}M_{\tilde{\chi}^0_1}(1 + \frac{P_{T}^2}{M_{\tilde{\chi}^0_1}^2})\right]^{1/2}.$$  

Since the momentum of the LSP is not constrained, the invariant mass distribution shows an edge at $\sim 100$ GeV.

III. BLACK HOLES AT THE LHC

In LED scenarios, $pp$ collisions at the LHC could produce TeV-mass BHs with characteristic lifetimes of $10^{-25}$ s [12,16]. Numerous studies have focused on BH signatures at the LHC [14] and various Monte Carlo generators are available for simulation purposes [22,32,33]. A quick look at BH production at the LHC reveals the following. According to Thorne’s hoop conjecture [35], a BH of mass $M$ is formed when an object is compressed in all directions such that

$$C < 2\pi R_s(M),$$

where $C$ is the circumference of the region where the object is compacted into and $R_s$ is the Schwarzschild radius for a BH of mass $M$. An upper limit on the BH mass is obtained by assuming no gravitational energy loss at formation, corresponding to the black disk (BD) cross section $\sigma_{BD} = \pi R_s^2$. A more realistic model assumes that all the center-of-mass energy is not available for BH formation, some being lost as gravitational radiation (see Ref. [36] for a more detailed discussion). To estimate the energy loss, the colliding particles are treated as two Aichelburg-Sexl shock waves [37]; the overlap of the shock waves forms a trapped-surface (TS) which sets a lower limit to the mass of the BH [38]. (For an alternative estimate of the collisional gravitational loss, see Ref. [39].) The cross section at the LHC involves summing up the contributions from all the initial partons. The cross section in the TS scenario is

$$\sigma_{pp\rightarrow BH}(s, n) = \sum_x \int_0^1 \int_0^1 dx \int_0^1 dx' f_i(x', Q) \times f_j(x/x', Q) F \sigma_{BD}(xs, n),$$

where $Q$ is four-momentum transfer squared, $f_i(x, Q)$ are the parton distribution functions, $z$ is the normalized impact parameter, and $F$ is a form factor. The cutoff in $x$ is related to the minimum allowed mass of the object, $M_{\text{min}}$, and the fraction of center-of-mass energy trapped in the BH, $\gamma(z)$, by $x_m = M_{\text{min}}/[s\gamma^2(z)]$. TeV BHs may carry electric or color charge and angular momentum. Immediately after formation, they are expected to decay through loss of excess multipole moments (balding phase), gravitational + Hawking radiation [40] (evaporation phase) and final $n$-body decay or remnant production (Planck phase). SM particles are emitted on the brane and can be detected [41]. Since the balding phase is poorly understood, simulations neglect the energy loss in this phase. The description of the evaporation phase is also approximated; since emissivities of rotating BHs are not known for all fields, BH generators use greybody factors for nonrotating BHs [42,43]. In CATfish, the total decay multiplicity is [22]

$$N = \frac{(n + 1)S}{4\pi} \sum_i c_i P_{\vec{r}_i} \Gamma_{\vec{r}_i} R_{\vec{r}_i},$$

where $c_i$ are the degrees of freedom of species $i$, $\Gamma_{\vec{r}_i}$ and $\Gamma_{\vec{r}_i}$ are the relative emissivities of Ref. [43], $S$ is the initial entropy of the BH, and $P_{\vec{r}_i}$ and $R_{\vec{r}_i}$ are spin-dependent normalization factors. A more detailed discussion of the evaporation and Planck phases of TeV BHs can be found in Refs. [12,16].

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1Recently, a new BH generator (BlackMax) appeared in the literature [34]. BlackMax is supposed to include BH rotational effects. However, the gravitational loss for rotating BHs is artificially set to zero. Since the energy loss due to gravitons is enhanced by rotation and extra-dimensional effects, and cannot be neglected, BlackMax results for rotating BHs should not be trusted.
Dilepton production in BH events differ greatly from dilepton production in the MSSM. Unlike SUSY, there is no single process of dilepton production; dileptons are either produced by the BH directly or by the decay of heavier particles such as the $Z_0$ boson, $t\bar{t}$ pairs of a combination of the two. Therefore, the BH dilepton invariant mass does not show a sharp cutoff at high energy.

### IV. EVENT SIMULATIONS

SUSY simulations are carried out using a combination of ISAJET and PYTHIA, with the former generating the mass spectrum. BH simulations are carried out using the CATFISH Monte Carlo generator. The setup for each simulation is summarized below:

1. **SUSY:**
   - (a) The MSSM mass spectrum is generated with ISAJET (ver. 7.75);
   - (b) The mass spectra in Supersymmetry Les Houches Accord format is fed into PYTHIA;
   - (c) All SUSY processes except SM Higgs production are simulated;
   - (d) Unstable SM particles and sparticles are hadronized or decayed with PYTHIA.

2. **BHs:**
   - (a) The cross section for a BH event is calculated in the center-of-mass frame;
   - (b) The initial BH mass is sampled from the differential cross section;
   - (c) The BH is decayed through Hawking mechanism and final $n$-body event (or remnant);
   - (d) Unstable quanta are hadronized or decayed with PYTHIA.

The benchmark model for SUSY is LHC point A. The parameters for the BH benchmark model are fundamental Planck scale $M_\ast = 1$ TeV, minimum BH mass $M_{\text{min}} = 2$ TeV, classical-to-quantum threshold $Q_{\text{min}} = 1$ TeV, six extra dimensions ($n = 6$) and two-body final decay ($n_p = 2$). Particles produced in the initial-radiation phase are removed by imposing $P_T$ cuts of 5 GeV and 15 GeV for leptons and photons + hadrons, respectively.

### V. EVENT ANALYSIS

In this section, we first use event-shape variables to discriminate SUSY and BH models. We then complement these results by looking at isolated dilepton events. The salient feature of this analysis is that BH events tend to be more spherical than SUSY events due to the spherical nature of the Hawking radiation. This is especially evident for high-mass BHs. The formation of a stable BH remnant at the end of the evaporation phase also helps to discriminate MSSM and BH events because of the large amount of energy which is carried away by the remnant. Isolated dilepton events provide a further powerful means to distinguish the two models. This is due to the fact that leptons are rarely emitted by BHs (the hadron-to-lepton ratio is approximately 5:1) and are uncorrelated; they can be emitted at any angle w.r.t. beam axis, whereas SUSY dileptons typically originate from a single decay chain.

#### A. $P_T$ and event-shape variables

Observation of events with large $P_T$ and multiple jets would provide a strong evidence for new physics at the TeV scale with little background. Figure 3 shows visible energy, missing transverse momentum, and transverse momentum of leptons and hadrons + photons for 10000 MSSM and BH benchmark events corresponding to an integrated LHC luminosity of $\sim 1$ pb$^{-1}$. Even in the absence of a BH remnant, the amount of visible energy and $P_T$ is comparable for the two scenarios. This is due to the presence of invisible channels in both models: the LSP for SUSY and neutrinos + gravitons for the BH. The flavor of the decay products is a better discriminator. MSSM interactions do not produce leptons with energy above the TeV since isolated leptons are produced by the decay of particles with typical energy of less than a few hundred GeV. On the contrary, quanta produced in the BH decay are characterized by an average energy $E \sim M/N$, where the multiplicity $N$ is less than 10 for typical BHs at the LHC. Since Hawking evaporation does not distinguish leptons from hadrons, hard leptons with energy up to several TeV are likely to be produced during the BH decay. This suggests that isolated leptons may provide a powerful means to discriminate the two models. This is indeed the case, as we shall see in the next section.

The four plots in the left panel of Fig. 4 show how variations in the BH Planck phase affect the observables of Fig. 3. The plots compare two- and four-body decays to the formation of a BH remnant ($n_p = 0$). By the time the remnant has formed, the BH is expected to have shed electric and color charges. (See, however, Ref. [44] for an alternative scenario.) If this is the case, the BH remnant is undetectable and a source of missing transverse momentum in addition to neutrinos and gravitons which are emitted during the Hawking evaporation phase. This leads to a larger difference in $P_T$ between the MSSM and BH models. The visible transverse momentum in hadrons + photons is sensibly reduced in the presence of a BH remnant; the latter carries away energy which otherwise would have been emitted in visible channels (mostly hadrons) during the BH decay phase. It is interesting to note that the amount of transverse momentum in the leptonic channel is essentially unaffected by the presence of a BH remnant. This is due to the fact that leptons are rarer than hadrons in the BH decay phase; variations in the energy distribution of the leptonic channel are thus suppressed compared to the hadronic channel. Changes in the number of final Planckian hard quanta do not produce significant differences in the distributions; more quanta of lower
energy behave statistically like less quanta with higher energy. Provided that the BH decays at the end of the Hawking phase, it is thus safe to set the number of Planckian quanta to $n_p = 2$ or $n_p = 4$, although BHs may decay in different numbers of particles on an event-to-event basis. Variations in the classical-to-quantum threshold $Q_{\text{min}}$ are also not expected to cause significant differences in the energy/momentum distributions. A higher threshold increases the emission in the Planck phase while decreasing Hawking radiation. Since these phases differ only in relative greybody factors, the effect is too small to be detected.

Event-shape variables such as sphericity and the 2nd Fox-Wolfram moment can be used to complement the above analysis. BH events are more spherical because of the nature of Hawking radiation and the “jetty” nature of SUSY decays. Formation of a BH remnant and high values of the fundamental scale lead to significant higher sphericity than SUSY (top panels of Fig. 5). The 2nd Fox-Wolfram moment (bottom panels of Fig. 5) is stable versus changes in the BH Planck phase and provides a good MSSM/BH discriminator. BH models with higher $M_s$ can be differentiated more easily from the MSSM. BH spin [45] is not expected to significantly change this conclusion; although rotation may affect the isotropy of Hawking radiation, most BHs are formed with low angular momentum and their plane of rotation lies on the brane. Therefore, the effect on the sphericity distribution of SM quanta should be small.

Similar conclusions can be reached by looking at jet masses and number of jets. The MSSM generates more and lighter jets than the BH model due to copious production of quarks (Fig. 6). The difference is again specially significant for high values of $M_s$ and in the presence of BH remnants. Absence of sub-$Q_{\text{min}}$ hard jets could provide strong evi-
FIG. 4 (color online). Distribution of visible energy, $p_T$, and transverse momenta of leptons and hadrons + photons. SUSY plots are shown as open squares. The four plots in the left panel show the effect of different decay modes in the Planck phase of ten-dimensional BHs: remnant formation ($n_p = 0$, filled triangles), two-body decay ($n_p = 2$, filled circles) and four-body decay ($n_p = 4$, filled squares). The fundamental Planck scale is $M_\gamma = 1$ TeV. The four plots in the right panel show the effect of varying the fundamental Planck scale: $M_\gamma = 1$ TeV (filled triangles), $M_\gamma = 2$ TeV (filled circles) and $M_\gamma = 3$ TeV (filled squares). The ten-dimensional BHs decay in two hard quanta at the end of the evaporation phase.

FIG. 5 (color online). Sphericity (top panels) and 2nd Fox-Wolfram moment (bottom panels) for 10 000 BH and MSSM events (open squares). The left panels show the effect of different Planckian decay modes: BH remnant (filled triangles), two-body decay (filled circles) and four-body decay (filled squares). The fundamental scale is $M_\gamma = 1$ TeV and the number of extra dimensions is six. The right panels show the effect of different fundamental scales: $M_\gamma = 1$ TeV (filled triangles), 2 TeV (filled circles) and 3 TeV (filled squares). The ten-dimensional BHs decay in two quanta at the end of the Hawking phase.
dence for BH remnant production. (See the suppression of heavy jets below the classical-to-quantum threshold $Q_{\text{min}} = 2$ TeV in the top leftmost panel of Fig. 6.)

B. Event analysis using high-$P_T$ dileptons

The use of isolated dileptons as SUSY signature has been extensively discussed in the literature [29,46]. Although their production is not as high as colored particles, high-energy isolated leptons provide a cleaner environment by allowing the removal of the QCD background. Moreover, since most of BHs produced at the LHC are expected to be very light, multiparticle analysis may not provide the most effective discriminators [22,47]. The study of leptonic final states alleviates this problem.

The dominant MSSM interaction for opposite-sign, same-flavor (OSSF) dileptons at LHC point A is [30] with a branching ratio of 27%. The maximum dilepton invariant mass for this interaction is

$$M_{ll}^{\text{max}} = m_{\tilde{\chi}_2^0} \left[ \left( 1 - \frac{m_2^2}{m_1^2} \right) \left( 1 - \frac{m_2^2}{m_1^2} \right) \right]^{1/2} \sim 100 \text{ GeV}.$$ 

The background for this process is due to SM decays of $W$, $Z$ bosons and top quarks. This background can be removed by applying suitable cuts on transverse momentum and sphericity of the leptons [25]:

(i) $P_{Tl} \simeq 15$ GeV, $|\eta_l| < 2.5$;

(ii) Isolation cut, $\sum_i P_{Ti} < 7$ GeV in a cone of $R = 0.2$,

where $P_{Tl}$ is the transverse momentum of the leptons, $R = \sqrt{\Delta \eta^2 + \Delta \phi^2}$, $\eta = -\ln[\tan(\theta/2)]$ is the pseudorapidity, and $\phi$ and $\theta$ are the azimuthal and polar angles of the lepton w.r.t. beam axis, respectively.

Isolated leptons in BH decays come directly from the BH itself, from the decay of $Z_0$ bosons and top quarks, or from a combination of the two. Since the branching ratio of $Z_0$ into leptons is small, $\Gamma(l^+ l^-)/\Gamma_{\text{tot}} \sim 0.034$ [48], and the decay of top quarks into leptons is rare [49], production of OSSF dileptons is less frequent in the BH model than in the MSSM. Our analysis shows that an OSSF dilepton event occurs approximately every $100$ BH and $20$ SUSY events, with a $\sim 1:5$ ratio of BH-to-SUSY dilepton events at fixed luminosity.

Figure 7 shows the dilepton invariant mass distribution for the MSSM (shaded plot) and the BH model with final two- and four-body decay (left and right panels, respectively). As expected, the SUSY distribution shows a sharp edge at $\sim 100$ GeV [25]. The BH invariant mass distribution is characterized by a peak at $\sim 90$ GeV and a long tail up to energy of several TeV. The peak is due to dilepton events produced from the decay of $Z_0$ bosons, the dominant channel for OSSF dilepton production in BH. The tail is originated by uncorrelated lepton pairs emitted directly by the BH or in top quark decays. The leptons are hard and the reconstructed dilepton mass can have super-TeV values.

The number of isolated, high-$P_T$ leptons can also be used to complement the dilepton analysis (left panel of Fig. 8). SUSY events are capable of producing up to five isolated leptons from the cascade decay of heavy spar-
ticles. Events with $\tilde{\chi}_2^0\tilde{\chi}_2^0$ or $\tilde{\chi}_1^\pm\tilde{\chi}_2^0$ may produce four or three isolated leptons, respectively [50]. On the contrary, events with three or more isolated leptons are very suppressed in BH decays at the LHC energy. Although multilepton events are rare, there is very little background and they could be effectively used to distinguish the MSSM and the BH model. Other effective discriminators can be constructed by looking at dilepton events with same sign and/or opposite-flavor leptons. The “democratic” nature of the BH decay makes all dilepton events roughly equally probable, whereas the MSSM favors same-flavor dileptons. The presence of hard opposite-flavor leptons is a clear indication of BH decay (right panel of Fig. 8). Our analysis shows that 73% of SUSY dilepton events are OSSF, compared to only 50% in the BH model. Conversely, opposite-flavor events are twice more frequent in the BH model (40%) compared to the MSSM (21%).

VI. CONCLUSIONS

We have discussed and compared the signatures of the MSSM and the TeV-BH model at the LHC. A thorough analysis of event-shape variables and dilepton events has shown that it is possible to distinguish the two models. BH events are characterized by higher sphericity than SUSY processes. If a BH remnant is formed at the end of the evaporation phase, missing $P_T$ and heavy jet mass are effective signatures to discriminate BH formation from the MSSM. Although event-shape variables alone cannot unequivocally discriminate between SUSY and BHs, their
knowledge may prove useful when combined with the analysis of the leptonic channel. Isolated dileptons could provide the “smoking gun” for detecting BHs at the LHC. The BH dilepton invariant mass shows a tail at high energy which is absent in the SM or MSSM. This analysis can be further strengthened by looking at the number and flavor of isolated leptons.

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