Dynamical Study of the Dissociative Chemisorption of CHD₃ on Pd(111)

Nick Gerrits,*† Helen Chadwick,** and Geert-Jan Kroes*†

1Gorlaeus Laboratories, Leiden Institute of Chemistry, Leiden University, P.O. Box 9502, 2300 RA Leiden, the Netherlands
2Department of Chemistry, Swansea University, Singleton Park, Swansea SA2 8PP, U.K.

ABSTRACT: The specific reaction parameter (SRP) approach to density functional theory has been shown to model reactions of polyatomic molecules with metal surfaces important for heterogeneous catalysis in the industry with chemical accuracy. However, transferability of the SRP functional among systems in which methane interacts with group 10 metals remains unclear for methane + Pd(111). Therefore, in this work, predictions have been made for the reaction of CHD₃ on Pd(111) using Born–Oppenheimer molecular dynamics while also performing a rough comparison with experimental data for CH₄ + Pd(111) obtained for lower incidence energies. Hopefully, future experiments can test the transferability of the SRP functional among group 10 metals also for Pd(111). We found that the reactivity of CHD₃ on Pd(111) is intermediate between and similar to either Pt(111) or Ni(111), depending on the incidence energy and the initial vibrational state distribution. This is surprising because the barrier height and experiments performed at lower incidence energies than investigated here suggest that the reactivity of Pd(111) should be similar to that of Pt(111) only. The relative decrease in the reactivity of Pd(111) at high incidence energies is attributed to site specificity of the reaction and to dynamical effects such as the bobsled effect and energy transfer from methane to the surface.

1. INTRODUCTION

An important heterogeneously catalyzed industrial process is steam reforming, where methane and steam react over a metal catalyst (typically Ni) and subsequently form carbon monoxide and hydrogen. At high temperature, the dissociation of methane, i.e., breaking the first CH bond, is a rate-controlling step in steam reforming on a wide variety of metals. Therefore, a detailed study of the CH bond breaking is warranted to improve catalysts. However, the reaction of molecules on metal surfaces remains difficult to simulate due to the complexity of molecule–metal surface interactions. The so-called specific reaction parameter (SRP) approach to density functional theory (DFT), though, has been shown to provide chemically accurate results, i.e., with errors smaller than 1 kcal/mol (4.2 kJ/mol), for a number of molecule–metal surface reactions. Within the SRP-DFT approach, two density functionals are mixed, of which one overestimates and one underestimates the reaction probability, according to an empirically determined parameter to create an SRP functional. Recently, an SRP functional was developed (the SRP32-vdW functional) that gave chemically accurate results not only for the molecule–surface reaction it was developed for (CHD₃ + Ni(111)) but also for methane interacting with a metal from the same periodic table group (CHD₃ + Pt(111)) and with a stepped surface of Pt (CHD₃ + Pt(211)). However, it remains unclear whether this transferability is common among all group 10 metals. Therefore, in this work, we perform predictive Born–Oppenheimer molecular dynamics (BOMD) calculations for CHD₃ + Pd(111) with the SRP32-vdW functional in the hope that future experiments will test the transferability of the SRP functional describing methane interacting with all group 10 metal surfaces. Although in our previous work, we usually referred to our direct dynamics calculations with SRP functionals as “ab initio molecular dynamics” (AIMD) calculations, we have changed our wording of the method from AIMD to BOMD as “ab initio” can be misleading in the context of calculations based on a semiempirical density functional.

To ensure the validity of the BOMD method, we address conditions for which the total energy of the molecule (translational + vibrational) exceeds the minimum zero-point energy corrected barrier height of the system addressed. This ensures that the accuracy of the quasi-classical trajectory (QCT) method used in the BOMD dynamics is not much affected by quantum effects like tunneling and classical artifacts like zero-point energy violation. Second, for laser-off conditions, we only address conditions where at least 60% of the incident CHD₃ is in its initial vibrational ground state, and in predictions for initial-state selective reaction, we only address CH stretch excited CHD₃ to avoid problems with artificial intramolecular vibrational relaxation that might otherwise affect QCT calculations. Third, we address surface temperatures (here, 500 K) well above the surface Debye temperature (140 ± 10 K for Pd(111)), thereby ensuring that the energy transfer between the molecule and...
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Table 1. Minimum Barrier Geometries of Methane on Ni(111), Pd(111), and Pt(111)\(^{12}\)\(^{13}\)\(^{30}\)

| surface  | site  | \(Z\) (Å) | \(r\) (Å) | \(\theta\) (deg) | \(\phi\) (deg) | \(r'\) (deg) | \(E_\text{f}^\ast\) (kJ/mol) |
|----------|------|--------|--------|-----------|-----------|--------|----------------|
| Ni(111)  | top  | 2.18   | 1.61   | 135.7     | 164.7     | 29.1   | 97.9 (85.3)    |
| Ni(111)  | fcc  | 2.09   | 1.63   | 128.5     | 157.3     | 30.7   | 121.1 (105.5)  |
| Ni(111)  | hcp  | 2.16   | 1.74   | 132.9     | 167.8     | 35.6   | 134.6 (120.7)  |
| Ni(111)  | bridge | 2.06 | 1.65   | 126.3     | 154.8     | 29.5   | 135.1 (120.5)  |
| Ni(111)  | t2f  | 2.07   | 1.90   | 126.5     | 171.1     | 45.3   | 99.1 (88.8)    |
| Ni(111)  | t2b  | 2.12   | 1.63   | 130.4     | 160.0     | 31.0   | 113.9 (99.1)   |
| Pd(111)  | top  | 2.23   | 1.61   | 135.9     | 165.0     | 29.1   | 84.1 (70.1)    |
| Pd(111)  | fcc  | 2.14   | 1.73   | 133.0     | 160.8     | 27.8   | 132.6 (116.9)  |
| Pd(111)  | hcp  | 2.18   | 1.75   | 133.8     | 161.5     | 27.7   | 133.6 (118.1)  |
| Pd(111)  | bridge | 2.14 | 1.76   | 130.8     | 161.9     | 31.1   | 125.6 (110.9)  |
| Pd(111)  | t2f  | 2.17   | 1.82   | 137.5     | 178.0     | 40.6   | 108.4 (96.1)   |
| Pd(111)  | t2b  | 2.18   | 1.76   | 132.8     | 165.8     | 33.0   | 132.5 (118.3)  |
| Pt(111)  | top  | 2.28   | 1.56   | 133.7     | 168.9     | 27.2   | 163.5 (145.8)  |
| Pt(111)  | fcc  | 2.47   | 1.91   | 139.7     | 166.9     | 35     | 78.7 (66.5)    |
| Pt(111)  | hcp  | 2.59   | 1.90   | 122.1     | 161.2     | 39.1   | 158.0 (144.7)  |
| Pt(111)  | bridge | 2.36 | 1.77   | 136.2     | 164.3     | 29.0   | 146.2 (128.1)  |
| Pt(111)  | t2f  | 2.31   | 1.64   | 149.5     | 179.2     | 29.7   | 117.7 (101.6)  |
| Pt(111)  | t2b  | 2.45   | 1.81   | 140.5     | 172.6     | 32.0   | 152.9 (136.5)  |

\(^{*}\)The zero-point energy corrected barriers are given in the brackets.

The reaction of methane on metal surfaces remains fundamentally important due to many dynamically interesting effects. For example, in partially deuterated methane, the CH bond can selectively be broken by exciting the CH stretch mode. Also, the dissociative chemisorption of methane is vibrational-mode-specific and the mode specificity is dependent on the metal surface. Moreover, steric effects play a significant role. Finally, the reaction of methane is site-specific. For all of these reasons, we will present in this work a detailed analysis of the results from the BOMD calculations and compare them to the results obtained on Pt(111) and Ni(111).

This paper is structured as follows. Section 2 will present the methods used in this work. In Section 3, the results are presented and discussed. Finally, in Section 4, a brief summary will be given.

2. METHOD

For the BOMD and electronic structure (DFT) calculations, the Vienna ab initio simulation package (VASP version 5.3.5) is used. The first Brillouin zone is sampled by a \(\Gamma\)-centered \(6 \times 6 \times 1\) \(k\)-point grid, and the plane wave basis set kinetic energy cutoff is 400 eV. Moreover, the core electrons have been represented with the projector augmented wave method. The surface is modeled using a four-layer \((3 \times 3)\) supercell, where the top three layers have been relaxed in the \(z\) direction and a vacuum distance of 13 Å is used between the slabs. Due to the computational cost, a small vacuum distance \((i.e., 13 \text{ Å})\) is required, which effectively raises the barrier height by 4.9 kJ/mol. Therefore, 4.9 kJ/mol is added to the translational energy to counteract this shift, as done earlier for, e.g., CHD\(_3\) + Ni(111). To speed up convergence, first-order Methfessel–Paxton smearing with a width parameter of 0.2 eV has been applied. The employed computational setup is confirmed to be converged within chemical accuracy (1 kcal/mol or 4.2 kJ/mol), as shown by convergence tests provided in the Supporting Information.

The transition state is obtained with the dimer method as implemented in the VASP transition-state tool package and is confirmed to be a first-order saddle point. Forces are converged within 5 meV/Å, where only the methane is relaxed.

We use the SRP32-vdW functional previously used for CHD\(_3\) + Ni(111), Pt(111), Pt(211), Pt(110), Pt(210), Cu(111), and Cu(211). The exchange functional is defined as

\[
E_x = x E_{x_{\text{PBE}}} + (1 - x) E_{x_{\text{RPBE}}}^\text{PBE}
\]

where \(E_{x_{\text{PBE}}}^\text{PBE}\) and \(E_{x_{\text{RPBE}}}^\text{PBE}\) are the exchange parts of the Perdew, Burke, and Ernzerhof (PBE) and revised PBE (RPBE).
exchange–correlation functionals, respectively, and $x = 0.32$. Since it has been shown that modeling van der Waals interactions is vital for describing the reaction of methane on a metal surface, the vdW correlation functional of Dion and co-workers (vdW-DF1) is used. A surface temperature of 500 K is simulated in the BOMD calculations, where the atoms in the top three layers are allowed to move and the expansion of the bulk due to the surface temperature is simulated by expanding the ideal lattice constant (3.99 Å) by a factor of 1.0049. The parameters used to simulate the molecular beams are taken from ref 13, which describes experiments performed for CHD$_3 +$ Pt(111). For every BOMD data point between 500 and 1000 trajectories were run, with a time step of 0.4 fs, for a maximum total time of 1 ps. A trajectory is considered to result in a reaction if a bond is 3 Å long, or longer than 2 Å for 100 fs, and in scattering if the molecule–surface distance is 6.5 Å and the velocity vector is pointing away from the surface. If neither has occurred after 1 ps, the trajectory is considered trapped. Other technical details of the BOMD calculations and the sampling of the initial conditions can be found in recent work.12,13,16,27

3. RESULTS

3.1. Activation Barriers. The barrier heights and geometries of CHD$_3$ on Pd(111) are compared to the barrier data on Ni(111) and Pt(111) in Table 1. $\theta$ is the angle between the dissociating bond and the surface normal, $\beta$ is the angle between the surface normal and the umbrella axis, which is defined as the vector going from the geometric center of the three nondissociating hydrogen atoms to the carbon atom, and $\gamma$ indicates the angle between the umbrella axis and the dissociating bond (see Figure 1). The minimum barrier even later. The distance of the carbon atom to the surface is smaller for Pd(111) and Ni(111) than at the top site, whereas in most cases, it is larger for Pt(111). The difference between the barrier heights obtained on Pd(111) and Ni(111) above these sites is considerably smaller than between the barrier heights at the top site. For Pt(111), the obtained barrier heights at the sites other than the top site are considerably higher than those of Pd(111) and Ni(111). The general trend observed here is that when going from Ni(111) to Pt(111), the difference between the barrier heights at the top site and at the other sites increases. We also note that, among the sites other than the top sites, the lowest barrier occurs on the t2f site for all metals. For Ni(111), this barrier is almost as low as the top site so that it may play an important role in the dynamics.

Finally, the adsorption energies of CH$_3$ and H on Pd(111) are compared to those on Ni(111) and Pt(111) in Tables 2 and 3. For CH$_3$, Pd(111) is an intermediate of Ni(111) and Pt(111) where the preferred sites are the hollow sites. This indicates the angle between the umbrella axis and the surface normal, $\gamma$ is the angle between the dissociating bond and the surface normal, $\theta$ is the angle between the surface normal and the umbrella axis, and $\beta$ is the angle between the surface normal and the umbrella axis, which is defined as the vector going from the geometric center of the three nondissociating hydrogen atoms to the carbon atom, and $\gamma$ indicates the angle between the umbrella axis and the dissociating bond (see Figure 1).

Figure 1. Transition state of methane on Pd(111), indicating the geometry angles as used in Table 1. $\theta$ is the angle between the CH bond and the surface normal, $\beta$ is the angle between the umbrella axis and the surface normal, and $\gamma$ is the angle between $\theta$ and $\beta$.

geometry on Pd(111) is similar to the minimum barrier geometry on Ni(111), with the main difference being that the barrier on Pd is at a larger distance from the surface than on Ni. However, the barrier height on Pd is much closer to that on Pt(111), being only 5.4 kJ/mol higher than on Pt(111). We based the minimum barrier heights reported in Table 1, we would expect the reactivity of Pd(111) to be closest to that of Pt(111). Furthermore, the minimum barrier is located on the top site, which is typical for methane on a metal surface.12,13,16,61

Moreover, barriers are also obtained above the fcc, hcp, bridge, top-2-fcc (t2f), and top-2-bridge (t2b) sites, by fixing the carbon in the X and Y directions above the aforementioned sites. For these barrier geometries, the angles are similar, but the dissociating bond length does increase, making the barrier

| surface | site | $Z_{cc}$ (Å) | adsorption energy (kJ/mol) |
|---------|------|--------------|-----------------------------|
| Ni(111) | bridge | 1.69 | −155.2 |
| Ni(111) | fcc | 1.55 | −175.2 |
| Ni(111) | hcp | 1.56 | −172.5 |
| Ni(111) | top | 1.98 | −143.9 |
| Pd(111) | bridge | 1.85 | −158.2 |
| Pd(111) | fcc | 1.75 | −160.5 |
| Pd(111) | hcp | 1.77 | −152.9 |
| Pd(111) | top | 2.09 | −188.4 |
| Pt(111) | bridge | 1.86 | −120.2 |
| Pt(111) | fcc | 1.78 | −115.2 |
| Pt(111) | hcp | 1.82 | −105.4 |
| Pt(111) | top | 2.10 | −180.8 |

*Note that the adsorption energies on Ni(111) and Pt(111) were calculated with the PBE functional.*

| surface | site | $Z_{cc}$ (Å) | adsorption energy (kJ/mol) |
|---------|------|--------------|-----------------------------|
| Ni(111) | bridge | 1.04 | −256.4 |
| Ni(111) | fcc | 0.91 | −270.2 |
| Ni(111) | hcp | 0.91 | −269.3 |
| Ni(111) | top | 1.47 | −212.8 |
| Pd(111) | bridge | 0.98 | −255.2 |
| Pd(111) | fcc | 0.81 | −268.0 |
| Pd(111) | hcp | 0.81 | −262.7 |
| Pd(111) | top | 1.56 | −223.9 |
| Pt(111) | bridge | 1.06 | −256.5 |
| Pt(111) | fcc | 0.92 | −261.3 |
| Pt(111) | hcp | 0.91 | −256.5 |
| Pt(111) | top | 1.56 | −257.2 |

*Note that the adsorption energies on Ni(111) and Pt(111) were calculated with the PBE functional.*

and 3. For CH$_3$, Pd(111) is an intermediate of Ni(111) and Pt(111). The difference between the adsorption energies at the hollow and top sites is smaller for Pd(111) than for Pt(111), but for both, the preferred site is the top site, as opposed to Ni(111) where the preferred sites are the hollow sites. This may also explain why the barrier for dissociation on the t2f site
is so low on Ni(111). However, Pd(111) is very similar to Ni(111) concerning the adsorption of hydrogen, where the binding of hydrogen to the top site is considerably weaker than to the other sites.

3.2. Sticking Probability. Results for the reaction of methane on Pd(111) using BOMD are compared to those on Ni(111) and Pt(111) in Figure 2 for laser-off conditions and \( \nu_1 = 1 \) (exciting the CH stretch mode with one quantum). Note that three additional points for Ni(111) have been calculated at \( \langle E_i \rangle = 71.4, 89.2, \) and 101.1 kJ/mol for \( \nu_1 = 1 \) using the same computational setup as in ref 12. Additionally, results for \( \langle E_i \rangle = 146.6 \) kJ/mol were obtained in the original work of ref 12 but have not been reported before because there were no experimental data for this incidence energy. Contrary to expectations based on the minimum barrier heights only (see Table 1), for laser-off conditions, the reaction probability on Pd(111) is similar to that on Ni(111). It should be noted that for Ni(111), a slightly higher surface temperature is used (550 K) than for Pd(111) and Pt(111) (500 K). However, this should not affect the results considerably as the surface temperature does not play a large role at high incidence energies, which will be discussed more in-depth in Section 3.4. For \( \nu_1 = 1 \) at lower incidence energy, the reaction probability is similar on all three systems investigated. Interestingly, on Pd(111), the reaction probability does not increase from 102 to 112 kJ/mol. It is possible that this is related to the site dependence of the reaction, which will be discussed later in Section 3.3. The generally much lower laser-off reactivity of Pd(111) compared to that of Pt(111) at high incidence energy is also consistent with the prediction that Pt–Cu(111) is much more reactive than Pd–Cu(111) at high incidence energies.\(^{27}\) Finally, the trapping probabilities are not included in the reaction probability, as they are smaller than 0.5%.

The bond selectivity is shown in Figure 3, where the fraction of CH bond cleavage under laser-off and state-resolved \( \nu_1 = 1 \) conditions is compared. When the CH stretch mode is excited, the dissociation of CHD\(_3\) is very selective toward CH cleavage, whereas under laser-off conditions, CH cleavage is close to statistical (25%). This is similar to what has been observed for CHD\(_3\) + Ni(111)\(^{12,30}\) and CHD\(_3\) + Pt(111).\(^{13}\) However, it remains unclear why on Pd(111) for laser-off conditions the fraction of CH cleavage is considerably lower for 112 kJ/mol compared to the other incidence energies under laser-off conditions. This may well be a statistical anomaly since a statistical analysis using Fisher’s exact test\(^{62}\) cannot reject the null hypothesis that the CH dissociation probability is the same for all incidence energies. We also note that at higher incidence energies and laser-off conditions the CH cleavage ratio is somewhat lower than 0.25, which we attribute to the presence of CD-excited vibrational states in the beam,\(^{12}\) also noting that there may be some artificial energy flow between these modes in classical dynamics calculations.

3.3. Dynamics during the Reaction. The angles as indicated in Figure 1 during the BOMD trajectories are shown in Figure 4 and Table 4 for the reacted trajectories. It is observed that both the initial \( \theta \) and \( \beta \) angles, i.e., the angles that describe the orientations of the dissociating bond and umbrella axis, are close to the transition-state geometry. Moreover, during the dynamics, a considerable amount of bending between the dissociating bond and umbrella axis (\( \gamma \))
observe this, see, e.g., Figure 5 for Ni(111), observing the role in the reaction of CHD$_3$ on group 10 metal surfaces can be expected to play similar roles. That the bobsled effect is observed for methane reacting on a group 10 metal surface (as can be seen in Figure 4) but also for methane reacting on Cu(111).27

Distance of the carbon atom to the surface when a bond dissociates. Both laser-off and $\nu_1 = 1$ trajectories that go on to react tend to slide off the MEP due to the bobsled effect and thus react over higher barriers. This deviation from the MEP increases with incidence energy, which is observed above all high-symmetry sites and thus is not related to the site over which the methane reacts. Furthermore, the bobsled effect is considerably smaller for Pt(111) than for Pd(111) and Ni(111), which leads to methane having to react over relatively higher barriers on Pd(111) and Ni(111) than on Pt(111).

For similar values of the reaction probability, the bobsled effect on the reaction dynamics of CHD$_3$ under laser-off conditions (predominantly $\nu_1 = 0$) is larger than for $\nu_1 = 1$. The reason is that larger incidence energy is required for $\nu_1 = 0$ to react than for $\nu_1 = 1$ so that $\nu_1 = 0$ CHD$_3$ tends to slide further of the minimum energy path than $\nu_1 = 1$ CHD$_3$. To observe this, see, e.g., Figure 5 for Ni(111), observing the differences between laser-off conditions and $\nu_1 = 1$ for the lowest incidence energy for which a laser-off result is available on the one hand and for the lowest incidence energy for which a $\nu_1 = 1$ result is available on the other hand, and Figure 2 to confirm that these conditions correspond to similar reaction probabilities. This has consequences for the vibrational efficacy, which is defined as the energy shift between the $\nu_1 = 1$ and $0$ ($\approx$ laser-off) reaction probability curves divided by the energy difference between $\nu_1 = 1$ and $0$, and defines how efficiently vibrational excitation promotes the reaction relative to increasing the translational energy. The larger bobsled effect on Ni(111) and Pd(111) than on Pt(111) partly explains why the vibrational efficacies for these systems (0.9–1.3 for Ni(111) and 0.7–0.9 for Pd(111)) exceed that obtained for Pt(111) (0.3–0.8, see Table S3, and also ref 12 for Ni(111) and ref 13 for Pt(111)). Furthermore, the large bobsled effect we find for CHD$_3$ on Ni(111) is in line with one of the explanations Smith et al.36 provided for the high vibrational efficacy of the asymmetric stretch mode of CH$_4$ reacting on Ni(111), i.e., that $\nu_3 = 1$ CH$_4$ reacts at the transition state, while $\nu_3 = 0$ CH$_4$ slides off the MEP and has to pass over a higher barrier. We note that in the modeling of the reaction the molecule should be allowed to slide off the MEP to account for the bobsled effect on the vibrational efficacy. One reason that a too low vibrational efficacy was obtained for $\nu_1 = 1$ CH$_4$ on Ni(111) in ref 64 may have been that the RPH calculations used a harmonic approximation for motion orthogonal to the MEP and an expansion in harmonic vibrational eigenstates with up to one quantum only in all modes combined. It is possible that such a limited expansion is not capable of describing the effect that the molecule may slide off the reaction path, as perhaps indicated by the reaction probability of methane in its vibrational ground state becoming smaller for particular incidence energies if the expansion is enlarged to also contain states with up to two vibrational quanta.

Previously, it was observed that the minimum energy path (MEP) on Pd(111) is less favorable from a dynamical point of view than on Pt(111) due to the fact that the MEP makes a sharper turn on Pd(111) than on Pt(111).27 Therefore, it is expected that at low incidence energies and $\nu_1 = 1$ where dynamical effects such as the bobsled effect are less important, the reactivity on Pd(111) is similar to that on Pt(111), whereas at higher incidence energies and laser-off conditions, dynamical effects cause the reactivity on Pd(111) to be similar to that on Ni(111) for the reaction of CHD$_3$ in its vibrational ground state (to which laser-off reaction bears a close resemblance at a low nozzle temperature).

Another important dynamical aspect of the reaction of methane is the energy transfer from the molecule to the surface.24 Figure 6 compares for scattered trajectories this energy transfer from CHD$_3$ to Cu(111),44 Pt(111),55 Ni(111),12 and Pd(111), where the energy transfer $E_T$ is defined as

$$E_T = (V_f + K_f) - (V_i + K_i)$$

(2)
where $V$ and $K$ are the potential free and kinetic energy of methane at the initial ($i$) and final ($f$) steps of the scattered trajectories, respectively. In general, it is observed that the lower the surface atom mass is, the higher the energy transfer is from methane to the surface. This is also predicted by the hard-sphere Baule model, where the mass ratio between the molecule and the surface atom plays a large role in the energy transfer. This energy transfer is described by

$$E_T = \frac{4\mu \cos^2 \gamma}{(1 + \mu)^2} E_i$$

(3)

where $\mu = m/M$ ($m$ is the mass of the projectile and $M$ is the mass of a surface atom) and $\gamma$ is the angle between the velocity vector of the molecule and the line connecting the centers of the hard spheres of the molecule and surface atom at impact. Surprisingly, the relatively simple Baule model does not only qualitatively but also semiquantitatively predict the energy transfer from methane to the metal surfaces, except for Ni(111), in contrast to what was previously predicted. Typically, the Baule model is actually taken as an upper limit by treating the collision as a head-on collision ($\gamma = 0$), from which one obtains the well-known Baule limit

$$E_T = \frac{4\mu}{(1 + \mu)^2} E_i$$

(4)

However, when an empirical average for the $\gamma$ angle distribution is used, in what we call the refined Baule model, the following average energy transfer (used in Figure 6) is obtained

$$\langle E_T \rangle = \frac{2.4\mu}{(1 + \mu)^2} E_i$$

(5)

Figure 6. Energy transfer from methane to Ni(111) (blue squares), Pd(111) (black circles), Pt(111) (red triangles), and Cu(111) (green diamonds) compared to the refined Baule model. The solid lines without symbols indicate results predicted by the refined Baule model, whereas the dashed and dotted lines with solid and open symbols indicate laser-off and $\nu = 1$ results, respectively.

Figure 7. Fraction of closest high-symmetry site (i.e., top, hollow, and bridge) to the impact site of reacting methane on Ni(111) (blue), Pd(111) (black), and Pt(111) (red) for laser-off and $\nu = 1$ as a function of the incidence energy when a bond dissociates, i.e., $r = r^\ddagger$. The dotted line indicates the statistical average for the high-symmetry site. The error bars represent 68% confidence intervals.

As can be seen from Figure 7, at high incidence energy, the site over which CHD$_3$ reacts on Pd(111) is close to statistical for both laser-off reaction and $\nu = 1$. However, at lower incidence energy, it is observed that the top site is the most reactive site, followed by the bridge site. This means that at lower incidence energy mostly only the minimum barrier is accessed, since it is located at the top site as discussed in Section 3.1. Therefore, at lower incidence energies, a large portion of the surface would be catalytically inactive. This corresponds with the lack of increase in the reactivity of $\nu = 1$ on Pd(111) from 102 to 112 kJ/mol, as it is also observed that the distribution of reaction sites shifts toward the less reactive sites (i.e., the bridge and hollow sites). Moreover, the reaction of CHD$_3$ on Pt(111) shows a similar site-specific behavior as CHD$_3$ reacting on Pd(111). At lower incidence energy, the reaction on Ni(111) again occurs predominantly over the top site; however, the second most reactive site is now the hollow site instead of the bridge site. In general, all of the considered metal surfaces show nonstatistical behavior, where the top site is usually favored, with the main difference being the ordering of the sites according to their reactivity. This behavior is also predicted by the site-specific barriers discussed in Section 3.1.

Considering the close to the spherical shape of methane, it is probable that the hard-sphere approximation made by the Baule model will typically hold. This is also suggested by Figure 6, which shows remarkably good agreement of the computed energy transfer with that predicted by the refined Baule model for Pt, Pd, and Cu. Additional work will be required to test the validity of the refined Baule model for other systems and investigate the considerably lower energy transfer we computed to Ni(111). Since the energy transfer from methane to Pd is higher than to Pt, less energy will be available for the reaction on Pd and thus the reaction probability should be further diminished on Pd compared to that on Pt. This effect will be larger at higher incidence energies as the difference in energy transfer between Pd and Pt will increase (see Figure 6). Moreover, as the energy transfer to Pd(111) and Ni(111) is expected to be equal, differences in reaction probabilities on Pd(111) and Ni(111) are most likely not caused by the energy transfer from methane to the metal surface.
of the reactivity is observed above the top site, whereas the hollow and bridge sites play a considerably smaller role. Here, the difference in reaction probability between Pd(111) and Pt(111) under laser-off conditions can be seen more clearly. The difference in reaction probability for the top site is large, whereas the difference for the hollow and bridge sites is generally much smaller. Therefore, the considerably lower reactivity of CHD$_3$ on Pd(111) than on Pt(111) under laser-off conditions is mostly due to the difference in the top-site reactivity. However, this difference is not caused by the difference in minimum barrier heights; probably, it is caused by the difference in barrier heights that can be dynamically accessed due to the bobsled effect. Furthermore, it remains unclear whether the large variation in reaction probability for Pd(111) and Ni(111) at the top site for $\nu_1 = 1$ is a statistical anomaly or a systematic feature. Also, the partial contribution of each site is compared to the total reaction probability for each surface in Figure S2, which again shows the aforementioned differences in site-specific reactivity.

While the difference between the low vibrational efficacy computed for CHD$_3$ + Pt(111) on the one hand and the higher vibrational efficacies on Pd(111) and Ni(111) on the other hand could be explained on the basis of the bobsled effect (see above), the reason for the higher vibrational efficacy on Ni(111) (0.9–1.3) than on Pd(111) (0.7–0.9, see Table S3) could not be explained in this way. On the basis of the minimum barrier heights and geometries collected in Table 1, it is tempting to speculate that the t2f site could play a role in this, as it has a much lower barrier on Ni(111) than on Pd(111), and a later barrier on Ni(111) than on Pd(111). The plot of the impact sites for the reactive trajectories with $E_r = 89 \text{ kJ/mol}$ for $\nu_1 = 1$ on Ni(111) (Figure S3) can be construed to offer some support for this idea, as quite a few reactive impacts are seen near the corners of the triangles making up the t2f and t2h sites. However, to gather further support for this idea, better statistics are needed, which could perhaps be obtained on the basis of QCT dynamics on a PES also incorporating the effect of surface atom motion.$^{14}$

In the reaction of CHD$_3$ on Pd(111), no steering in the xy plane is observed (on average, a movement of 0.06 Å in the xy plane), as is typical for the reaction of CHD$_3$ on a metal surface.$^{5,12,27,51,52}$ As a result, it should be a good approximation to treat the reaction with a sudden approximation for motion in X and Y, as done, for instance, with the RPH model of Jackson and co-workers,$^5$ and firmly established to be valid for CH$_4 + \text{Ni}(111),$$^{68}$ and also for H$_2$O + Ni(111).$^{69}$

Finally, we will summarize the general trends observed and how they affect the reaction probability, which are also shown in Table 5. First, the bobsled effect is considerably more important for Pd(111) and Ni(111) than for Pt(111), making Pt(111) considerably more reactive than the other surfaces, especially for laser-off conditions. Moreover, the energy transfer of methane to Pt(111) is smaller than to Pd(111) and Ni(111), again making Pt(111) relatively more reactive. However, the site-specific reactivity is increasingly more important when going from Ni(111) to Pt(111), reducing the reaction probability on Pt(111) the most. The vibrational efficacy plays an increasingly more important role when going from Pt(111) to Ni(111), increasing the reaction probability for $\nu_1 = 1$ on Ni(111) the most. Furthermore, the initial angular distribution of the molecule and concomitant steering are equally important on all surfaces considered here. These dynamical effects combined cause the reaction probability on Ni(111) and Pd(111) to be similar and on Pt(111) comparatively higher, for laser-off conditions. Additionally, they explain why the reactivity is rather similar on all of these surfaces for $\nu_1 = 1$. In this, we suspect that the site specificity plays the most important role in almost equalizing laser-off reaction on Pd(111) and Ni(111), while the vibrational efficacy should also be important to making the $\nu_1 = 1$ reaction probabilities almost equal on these two surfaces.

Due to the combined effects of decreased site specificity and increased vibrational efficacy, it is conceivable that Ni(111) becomes more reactive than Pd(111), and/or Pd(111) becomes more reactive than Pt(111) toward $\nu_1 = 1$ CHD$_3$ at higher incidence energies than results are shown for in Figure 2b. It would be a considerable challenge to explore this experimentally, for reasons,$^{70,71}$ (i) at higher incidence energies, the extraction of the reactivity of $\nu_1 = 1$ CHD$_3$ requires a subtraction of an increasingly large "laser-off" signal from a "laser-on" signal that might actually decrease, because laser excitation takes place from a rotational level that is less

![Figure 8. Reaction probability of CHD$_3$ on the high-symmetry sites (i.e., top, hollow, and bridge) on Ni(111) (blue), Pd(111) (black), and Pt(111) (red) for laser-off and $\nu_1 = 1$ as a function of the incidence energy when a bond dissociates, i.e., $r = r^*$. The error bars represent 68% confidence intervals.](https://example.com/figure8)
populated at the higher associated $T_n$ and (ii) the extraction requires the approximation that the reactivity of the vibrational ground state equals that averaged over the vibrational states populated in the beam under laser-off conditions, of which the validity decreases with incidence energy.

3.4. Discussion of Reactivity of Pd(111) vs Ni(111) and Pt(111); Comparison with Experiment. Experimentally, at low incidence energies (<70 kJ/mol) (see Figure 9), the reactivity of Pd(111) toward CH$_4$ is similar to that of Pt(111), whereas Ni(111) is about 3 orders of magnitude less reactive than Pt(111).$^{23,72}$ It should be noted that the experiments at low incidence energies were performed with CH$_4$ using various nozzle and surface temperatures (see Table 6), making a direct quantitative comparison between the experiments on CH$_4$ + Pt(111) and CH$_4$ + Pd(111) and with the BOMD results for CHD$_3$ difficult. Therefore, we will discuss the general trends observed for the reaction of methane on Pt(111) and try to extrapolate this to Pd(111).

In Figure 9b, a few results concerning Pt(111) and Pd(111) are shown to qualitatively compare the effect of nozzle and surface temperatures, and the isotopic effect of using CH$_4$ or CHD$_3$. Nattino et al.$^{16}$ used CHD$_3$ seeded in a He beam with $T_n = 120$ K, whereas Migliorini et al.$^{13}$ used CHD$_3$ seeded in a H$_2$ beam with $T_n = 500$ K. Typically, at the high incidence energies and reaction probabilities involved here, the surface temperature does not play a large role for the reactivity of methane.$^{53,73,76}$ Moreover, at high surface temperature, the seeding gas influences the kinetic energy and thus also the required nozzle temperature. Therefore, the slightly higher reaction probability of Nattino and co-workers$^{16}$ in the overlapping regime is caused by the higher nozzle temperature (as needed by He-seeded molecular beam studies) as a larger fraction of CHD$_3$ in the beam will be vibrationally excited.

However, the surface temperature can cause the reaction probability at lower incidence energy to vary by up to 2 orders of magnitude, depending on the surface temperature and incidence energy.$^{54,64,73,76,77}$ This surface temperature effect probably causes the reaction probabilities obtained by Luntz and Bethune$^{73}$ ($T_s = 800$ K) to be considerably higher than those obtained by Oakes and co-workers$^{74}$ ($T_s = 550$ K) and Bisson and co-workers$^{72}$ ($T_s = 600$ K), whom all used CH$_4$. On the other hand, the higher reaction probability obtained by Oakes et al. ($T_s = 500–1000$ K) compared to that by Bisson et al. ($T_s = 323–373$ K) is probably due to the higher employed nozzle temperature used by Oakes et al.

Furthermore, the effect of partially deuterating methane can be seen by comparing the results of Nattino et al. and Oakes et al. For the incidence energy range where data are available for both sets, the difference in surface temperature (i.e., $T_s = 120$ and 550 K, respectively) should only play a role for the low incidence energies. Moreover, the nozzle temperature employed by Nattino et al. is similar to that by Oakes et al. and thus should not make a large difference either. It is expected that these differences should also (partially) cancel out at high incidence energies. It has also been shown previously that using CHD$_3$ instead of CH$_4$ lowers the reaction probability.$^{73,78–80}$ However, the reaction probabilities obtained by Nattino et al. and Oakes et al. at high incidence energy are similar, where it is expected that the reaction probabilities obtained by Oakes et al. should be slightly higher than those by Nattino et al. It remains unclear why no difference at high incidence energy is observed between the two data sets, although it is possible that the molecular beams are considerably different making direct comparison difficult.

Finally, the reaction probability of CH$_4$ on Pd(111) obtained by Tait et al.$^{23}$ is similar to that of Oakes et al. for CH$_4$ + Pt(111), except for the highest incidence energies where Pd(111) is measured to be more reactive than Pt(111) toward methane. Both used the same surface temperature and similar nozzle temperature range, but Tait et al. used relatively less seeding gas and thus a higher nozzle temperature is employed for given incidence energy compared to Oakes et al., which perhaps explains the higher reaction probability for

![Figure 9](https://example.com/figure9.png)

**Figure 9.** (a) Experimental reaction probability of CH$_4$ on Ni(111) (blue), Pd(111) (black), and Pt(111) (blue) under laser-off conditions. Results for Ni(111) and Pt(111) are taken from ref 72 and refs 72–74, respectively. The Pd(111) results (black circles and triangles) are taken from ref 23, where the circles and triangles indicate incidence angles of 0 and 28°, respectively, and the black line is a linear regression fit those points. (b) Reaction probability of CH$_4$ and CHD$_3$ on Pd(111) and Pt(111) obtained with experiment (closed symbols) and BOMD (open symbols) under laser-off conditions. For CH$_4$ + Pt(111), only the results from ref 74 are shown. The red squares and diamonds indicate results for CHD$_3$ + Pt(111) taken from refs 16 and 13, respectively.

| System          | Refs       | Seeding gas | Surface temperature (K) | Nozzle temperature (K) |
|-----------------|------------|-------------|-------------------------|------------------------|
| CH$_4$ + Ni(111) | Bisson et al.$^{72}$ | H$_2$       | 475                     | 323–373                |
| CH$_4$ + Pd(111) | Tait et al.$^{23}$ | He          | 550                     | 470–885                |
| CH$_4$ + Pt(111) | Luntz et al.$^{73}$ | H$_2$, H$_2$, Ar | 800                     | 300                    |
| CH$_4$ + Pt(111) | Oakes et al.$^{13}$ | He          | 550                     | 500–1000               |
| CH$_4$ + Pt(111) | Bisson et al.$^{72}$ | H$_2$       | 600                     | 323–373                |
| CHD$_3$ + Pt(111) | Nattino et al.$^{16}$ | He          | 120                     | 500–850                |
| CHD$_3$ + Pt(111) | Migliorini et al.$^{13}$ | H$_2$ | 500                     | 400–650                |
Pd(111) at high incidence energy. At energies that are higher than those for which CH$_4$ + Pd(111) experimental results are available, our BOMD calculations predict a substantially lower reactivity of Pd(111) toward CHD$_3$ than that of Pt(111). While this may seem odd in light of the experimental results for CH$_4$ on Pt(111) and Pd(111), one should keep in mind that due to the simulated use of H$_2$ seeding the incidence energy is higher while the nozzle temperature is lower for the calculations on CHD$_3$ + Pd(111) and Pt(111), which leads to a larger importance of the bobsled effect and to a smaller importance of the promotion of reaction by vibrational excitation. Both effects disfavor the reaction on Pd(111). Nevertheless, experiments are clearly needed to verify our predictions for the reaction of CHD$_3$ toward CHD$_3$. For all of these reasons, we conclude that, experimentally, it is expected that the reactivity of CHD$_3$ + Pd(111) should be slightly lower than that of CHD$_3$ + Pt(111) at lower incidence energies. Qualitatively, this is also what we obtain from the BOMD calculations at higher incidence energies, although there the difference in reactivity is larger (see Figure 2).

4. CONCLUSIONS

In this work, predictive calculations using BOMD have been performed for CHD$_3$ on Pd(111) with the SRP32-vdW functional. The reactivity of Pd(111) is compared to those of Pt(111) and Ni(111) and is found to be intermediate between these systems. Although this is to be expected from the minimum barrier heights and experiments at low incidence energy, the reaction probability is also found to be dependent on dynamical effects such as the bobsled effect and energy transfer from methane to the metal surface. In general, at the lowest incidence energy and laser-off conditions when these dynamical effects are smaller, the reaction probability on Pd(111) is comparable to that on Pt(111), which is also observed by experiment. However, at higher incidence energies, these dynamical effects play a larger role and the reaction probability is more comparable to Ni(111). Furthermore, for $\nu_{\text{vib}} \approx 1$, all three systems investigated show similar reaction probabilities. Moreover, barriers across the surface need to be considered as the reaction of methane on a group 10 metal surface is highly site-specific, with the minimum barrier height and geometry varying across the surface. This variation in barrier heights across the surface also explains the similarity of the reactivity of Ni(111) and Pd(111) toward methane at high incidence energy. Interestingly, methane on Pd(111) and Ni(111) exhibits typically quite similar dynamical behavior such as the bobsled effect, energy transfer from methane to the surface, and the site-specific reactivity, whereas the dynamical behavior of methane on Pt(111) tends to be different from the aforementioned metal surfaces. This again causes reactivity of Pd(111) toward methane to shift more to that of Ni(111) than that of Pt(111). Our results also suggest why Pt–Cu(111) is predicted to be much more reactive than Pd–Cu(111) at high incidence energy. We hope that these predictions will inspire new experiments that will test the transferability of the SRP32-vdW functional to CHD$_3$ + Pd(111).

ASSOCIATED CONTENT

Supporting Information

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