Determining the Nature of Late Gunn–Peterson Troughs with Galaxy Surveys

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Abstract

Recent observations have discovered long (up to ~110 Mpc/h), opaque Gunn–Peterson troughs in the z ~ 5.5 Lyα forest, which are challenging to explain with conventional models of the post-reionization intergalactic medium. Here, we demonstrate that observations of the galaxy populations in the vicinity of the deepest troughs can distinguish two competing models for these features: deep voids where the ionizing background is weak due to fluctuations in the mean free path of ionizing photons would show a deficit of galaxies, while residual temperature variations from extended, inhomogeneous reionization would show an overdensity of galaxies. We use large (~550 Mpc/h) semi-numerical simulations of these competing explanations to predict the galaxy populations in the largest of the known troughs at z ~ 5.7. We quantify the strong correlation of Lyα effective optical depth and galaxy surface density in both models, and estimate the degree to which realistic surveys can measure such a correlation. While a spectroscopic galaxy survey is ideal, we also show that a relatively inexpensive narrowband survey of Lyα-emitting galaxies is ~90% likely to distinguish between the competing models.

Key words: dark ages, reionization, first stars – galaxies: high-redshift – intergalactic medium

1. Introduction

The reionization of the universe was the last major phase transition of baryons. The measured large-scale polarization of the cosmic microwave background (CMB) constrains the epoch of reionization to a characteristic redshift of z ~ 7–8 (Planck Collaboration et al. 2016a), and observations of transmission in the Lyα forest suggest that it has ended by z ~ 6 (Fan et al. 2006; McGreer et al. 2011; McGreer et al. 2015).

Above z ~ 5.5, the Lyα forest begins to exhibit large-scale (>50 Mpc/h) regions with transmission consistent with zero, commonly known as Gunn–Peterson (GP) troughs due to their similarity with expectations for a fully neutral IGM (Gunn & Peterson 1965). However, saturated absorption in the Lyα forest only requires volume-averaged hydrogen neutral fractions of x_HH1 ~ 10^{-4}, so the presence of these troughs does not unambiguously indicate a neutral IGM (Fan et al. 2006). GP troughs at z ~ 5.5 are not ubiquitous: the opacity of the Lyα forest, typically quantified by the effective optical depth \( \tau_{\text{eff}} \equiv -\ln(F) \) (where \( F \) is the mean transmitted flux), measured on scales of ~50 Mpc/h, varies considerably between different lines of sight (Fan et al. 2006).

Early studies suggested that these variations were consistent with expectations from the nonlinear connection between the density field of the IGM and the Lyα forest \( \tau_{\text{eff}} \) (Lidz et al. 2006). However, more recent work by Becker et al. (2015, henceforth B15) added new lines of sight to the original Fan et al. (2006) sample, and found that above z ~ 5.5 the variations in \( \tau_{\text{eff}} \) are substantially stronger than the expectations from the density field alone, implying large fluctuations in the neutral hydrogen fraction (x_HH1). Most notably, B15 discovered a ~110 Mpc/h GP trough from z ~ 5.52–5.88 (\( \tau_{\text{eff}} \geq 7.4 \) at 2\( \sigma \)) in a deep spectrum of the quasar ULAS J0148+0600 (zQ = 5.98). At these redshifts, the IGM appears to be predominantly highly ionized, and a model-independent analysis of dark regions in the Lyα and Lyβ forests suggests that reionization is complete (McGreer et al. 2011; McGreer et al. 2015). Indeed, B15 found that the ULAS J0148+0600 trough has significant (albeit weak) transmission throughout the Lyβ forest, so it is unlikely that the trough as a whole represents a not-yet-reionized patch of neutral gas.

The opacity of the ionized IGM at z \( \gtrsim 5.5 \) is closely linked to the neutral fraction of gas at low density (\( \Delta \equiv \rho/\bar{\rho} < 1 \)), where \( \bar{\rho} \) is the cosmic mean density; see, e.g., Oh & Furlanetto (2005). The equilibrium neutral fraction at fixed gas density is a function of two quantities: the photoionization rate of hydrogen \( \Gamma_{H I} \), and the gas temperature \( T \), where \( x_{H H1} \propto \Gamma_{H I}^{-1} T^{-0.7} \). Thus, stronger than expected (i.e., not directly due to the density field) variations in \( \tau_{\text{eff}} \) are either due to large fluctuations in the ionizing background or in the temperature of the IGM. In particular, the environment of the giant GP trough in B15 either has a weak ionizing background or is much colder than the typical IGM.

B15 showed that simple models for fluctuations in the ionizing radiation field due to the clustering of galaxies and a spatially uniform mean free path of ionizing photons (\( \lambda_{\text{mfp}} \)) were unable to reproduce the giant GP trough in ULAS J0148+0600, while remaining in agreement with the \( \tau_{\text{eff}} \) in the typical Lyα forest at z ~ 5.7. Davies & Furlanetto (2016, henceforth DF16) expanded upon the radiation field modeling of B15 by introducing spatial variations in \( \lambda_{\text{mfp}} \). Fundamentally, \( \lambda_{\text{mfp}} \) represents absorption of ionizing photons by residual neutral hydrogen in the IGM, so a stronger (weaker) ionizing background should result in a longer (shorter) \( \lambda_{\text{mfp}} \) due to the change in x_HH1. DF16 applied the analytic model of Quinn et al. (2011) to self-consistently compute ionizing background and \( \lambda_{\text{mfp}} \) fluctuations in a large semi-numerical simulation of the IGM. The enhanced fluctuations in the ionizing background due to \( \lambda_{\text{mfp}} \) fluctuations were able to reproduce the observed distribution of \( \tau_{\text{eff}} \), provided the average \( \lambda_{\text{mfp}} \) was smaller by a factor of two than an extrapolation from \( \lambda_{\text{mfp}} \) measurements at z ~ 2.5–5.2 (Worseck et al. 2014; D’Aloisio et al. 2018). Giant

5 This discrepancy can be accounted for by a likely bias in the \( \lambda_{\text{mfp}} \) measured along quasar sightlines at z ~ 5 (see D’Aloisio et al. 2018 for details).
GP troughs in this model result from large-scale voids which are
distant from sources of ionizing photons, and thus whose local \( \lambda_{\text{mfp}} \) is very short, strongly suppressing the ionizing
background (see also Crociani et al. 2011).

The process of reionization deposits a substantial amount of
thermal energy into the IGM from excess energy in newly
photoionized gas, leading to (initially) isothermal post-
reionization gas temperatures of \( \sim 1-4 \times 10^4 \text{ K} \) depending on
the nature of ionizing photon sources (Miralda-Escudé & Rees 1994; Abel & Haehnelt 1999; McQuinn 2012; Davies et al. 2016). The gas then cools, predominantly through inverse
Compton scattering off of the CMB and adiabatic cooling from the
expansion of the universe, such that by \( z \lesssim 5 \) the thermal state of the IGM is largely independent of the details of the
reionization process (Theuns et al. 2002; Hui & Haiman 2003,
although see Trac et al. 2008; Cen et al. 2009). However, the
typical cooling timescale is of order the Hubble time, so if
reionization ended as late as \( z \sim 6 \) there may be substantial
residual heat present in the IGM at \( z \sim 5.5 \). Additionally,
because the reionization process is inhomogeneous on large
\((\gtrsim 10 \text{ Mpc})\) scales (Furlanetto et al. 2004), this residual heat
could vary greatly between different regions of the universe.
D’Aloisio et al. (2015) investigated the possibility of large-

scale residual temperature fluctuations from the inhomoge-
neous reionization process as the source of large variations in
\( \tau_{\text{eff}} \) through the temperature dependence of the hydrogen recombination rate. D’Aloisio et al. (2015) found that
temperature fluctuations from a hot \((\Delta T = 3 \times 10^4 \text{ K})\) and extended \((z \sim 13-6)\) epoch of reionization were sufficient to
source the large observed scatter in \( \tau_{\text{eff}} \). In their model, large
regions with high \( \tau_{\text{eff}} \) are overdense regions which reionized
early, thus they have had more time to cool than the
typical IGM.

An alternative source of strong fluctuations in the ionizing
background (and thus, \( \tau_{\text{eff}} \) ) could instead be a sparsity of ionizing sources relative to the mean free path (Zuo 1992; Meiksin & White 2003), e.g., if the ionizing background is
dominated by luminous quasars (Chardin et al. 2015). Even this
model, however, appears to require coupled fluctuations of the
mean free path and ionizing background to be consistent with
observations (Chardin et al. 2017). Constraints from the
thermal state of the IGM at lower redshift and helium
reionization suggest that a large contribution to the ionizing
photon budget from quasars at \( z \gtrsim 5 \) is unlikely (D’Aloisio et al. 2017). For simplicity, we do not explore it further in this
work. Finally, we note that Gnedin et al. (2017) examined the
sensitivity of reionization models to other Ly\( \alpha \) forest statistics,
including the distribution of dark gap lengths and the characteristics of transmission peaks. In this work, we will
focus primarily on the \( \tau_{\text{eff}} \) measurements from Fan et al. (2006)
and B15.

Thus, we can make two opposing predictions for the
environment of the giant GP trough in ULAS J0148+0600:
either the region is underdense and has a much weaker ionizing
background than average (DF16, D’Aloisio et al. 2018), or the
region is overdense and is much cooler than average (D’Aloisio
et al. 2015). In this work, we study the implications of these
two models on the cross-correlation between GP troughs and
their local galaxy populations, with particular focus on the
giant GP trough in ULAS J0148+0600. In Section 2, we
describe our semi-numerical modeling of ionizing background
and temperature fluctuations in a \( \sim 550 \text{ Mpc}/h \) cosmological
volume and their resulting distributions of \( \tau_{\text{eff}} \) at \( z \sim 5.7 \). In
Section 3, we predict the distribution of UV-bright galaxies,
abundance matched to dark-matter halos in our semi-numerical
simulation, in large GP trough environments in the two
scenarios. In Section 4, we make similar predictions for Ly\( \alpha \)-
emitting galaxies by applying the conditional Ly\( \alpha \) equivalent
width model of Dijkstra & Wyithe (2012). Finally, in Section 5,
we conclude with a summary and prospects for other methods.

In this work, we assume a \( \Lambda \text{CDM} \) cosmology with \( h = 0.7, \Omega_m = 0.3, \Omega_L = 0.7, \Omega_b = 0.048 \) and \( \sigma_8 = 0.82 \). Distance
units are comoving unless specified otherwise.

2. Semi-numerical Modeling of \( \tau_{\text{eff}} \) Fluctuations

In this work, we used the semi-numerical code DEXM
(Mesinger & Furlanetto 2007) to produce a model for the
density field of the IGM at \( z = 5.7 \). We generated a 4096\(^3\)
realization of cosmological initial conditions (ICs) in a volume
546 Mpc/\( h \) on a side. We then quasi-linearly evolved the ICs to
\( z = 5.7 \) using the Zel’dovich approximation (Zel’dovich 1970)
onto a coarser 2048\(^3\) grid including the oversampling
prescription of DF16 to reduce shot noise in the evolved
density field. The left panel of Figure 1 shows a 50 Mpc/\( h \-

thick slice of the density field.

2.1. Fluctuations in the Ionizing Background
due to \( \lambda_{\text{mfp}} \) Fluctuations

To compute large-scale fluctuations in the ionizing back-
ground in our cosmological volume, we employed the method
of DF16, which we briefly summarize here. Dark matter halos
with masses greater than \( M_{\text{min}} = 2 \times 10^6 M_\odot \) were located in
the volume using an excursion-set-like procedure on the ICs
linearly evolved to \( z = 5.7 \) (Mesinger & Furlanetto 2007),
and then their positions were updated using the same Zel’dovich
displacement field that was used to evolve the density field.
Rest-frame UV luminosities (i.e., galaxies) were assigned to
each halo by abundance matching \(^5\) (e.g., Vale & Ostriker 2004)
to the measured UV luminosity function \(^6\) of Bouwens et al.
(2015), with our minimum halo mass corresponding to
\( M_{\text{UV, max}} \approx -12.9 \). The distribution of \( M_{\text{UV}} < -20 \) galaxies
in a 50 Mpc/\( h \)-thick slice of the simulation is shown in the
right panel of Figure 1, demonstrating their highly clustered
nature.

We further assume that the ionizing luminosity of each galaxy
is proportional to its UV luminosity, and leave the ratio of
ionizing-to-UV luminosity as a free (but constant) parameter
that we tune to match the measured \( \Gamma_{\text{HI}} \sim 3 \times 10^{-13} \text{ s}^{-1} \) at \( z \sim 5.7 \)
(D’Aloisio et al. 2018; Davies et al. 2018). The spatially variable
opacity of the IGM, parameterized by \( \lambda_{\text{mfp}} \), was assumed to
follow the relation \( \lambda_{\text{mfp}} \propto \Gamma_{\text{HI}}^{-3/2} \Delta^{-1} \), motivated by analytic
arguments in McQuinn et al. (2011, see the discussion in DF16
for details). We adopt \( \lambda_{\text{mfp}} (\Gamma_{\text{HI}} = 1 \text{ \&} \Delta = 1) = 15 \text{ Mpc} \),
which DF16 found was required to explain the distribution in \( \tau_{\text{eff}} \)
measured by B15 at \( z \sim 5.6 \). With this \( \lambda_{\text{mfp}} \), reproducing the
measured \( \Gamma_{\text{HI}} = 3 \times 10^{-13} \text{ s}^{-1} \) requires an (escaping) ionizing-
to-UV luminosity ratio of \( \sim 0.1 \). Assuming \( f_{\text{esc}} = 0.2 \) (e.g.,
Robertson et al. 2015) would imply an intrinsic ionizing-to-UV

\(^5\) This minimum halo mass was chosen for consistency with DF16.

\(^6\) The star formation efficiency of dark-matter halos implied by this approach
appears to be reasonable at high redshift (Mirocha et al. 2017).

\(^7\) In detail, we interpolate between the \( z \sim 5.9 \) and \( z \sim 4.9 \) luminosity
functions to estimate the luminosity function at \( z = 5.7 \).
The luminosity ratio of $\sim 0.5$ which, while fairly high, is still allowed by state-of-the-art population synthesis models (Stanway et al. 2016).

The ionizing background was then iteratively computed on a $156^3$ grid, corresponding to the same 5 Mpc resolution as DF16. We show a slice of the $\Gamma_{\text{HI}}$ field in the left panel of Figure 2, demonstrating correlated fluctuations on scales as large as $\sim 100$ Mpc/h. In this model, overdense regions have an enhanced $\Gamma_{\text{HI}}$, while voids have a very weak $\Gamma_{\text{HI}}$. The inclusion of $\lambda_{\text{mfp}}$ fluctuations is critical to the magnitude of this effect, especially in weakening the radiation field in void environments.
depth for this reionization history is $D$ and redshift to produce an ionization history very similar to that in the excursion-set model. While underdense regions are reionized later, following the generic predictions of inside-out reionization in the excursion-set model.

2.2. Fluctuations in IGM Temperature due to Inhomogeneous and Extended Reionization

We model post-reionization fluctuations in the temperature of the IGM using a procedure similar to D’Aloisio et al. (2015), but in a semi-numerical fashion more analogous to the method of Lidz & Malloy (2014). We compute the reionization redshift field ($z_{\text{reion}}$) in our cosmological volume on a $1024^3$ grid by computing excursion-set reionization maps in DEXM from $z = 5.8–13.0$ in steps of $\Delta z = 0.1$. For computational efficiency, we computed the reionization maps using settings in DEXM that mimic the code 21CMFAST (Mesinger et al. 2011); that is, the fraction of material in collapsed objects was computed analytically from the density field itself rather than the halo field, and we adopt the central-pixel-flagging algorithm instead of the slower bubble-painting algorithm (see Zahn et al. 2011 for a discussion of the relative accuracy of these methods). The minimum halo mass for producing ionizing photons was fixed to $M_{\text{min}} = 2 \times 10^9 M_{\odot}$, for consistency with the halos in the ionizing background model, and the ionizing efficiency $\eta$ was tuned as a function of redshift to produce an ionization history very similar to that in D’Aloisio et al. (2015): reionization begins at $z \sim 13$, and then $\eta_{\text{HI}}(z)$ evolves roughly linearly with redshift until reionization is largely complete by $z \sim 6$. The Thomson scattering optical depth for this reionization history is $\tau_e = 0.07$, within $2\sigma$ of the most recent constraints from Planck (Planck Collaboration et al. 2016b). A slice of the resulting reionization redshift field is shown in Figure 3 (compare with the left panel of Figure 3 in D’Aloisio et al. 2015).

To compute the residual temperature field at $z = 5.7$, we employ a simple temperature evolution model similar to that described in Upton Sanderbeck et al. (2016). We assume that, at $z = z_{\text{reion}}$, each cell in our cosmological volume is heated to $3 \times 10^4$ K. The temperature evolution of gas in the IGM is then evolved as (Hui & Gnedin 1997; Furlanetto & Oh 2008; Upton Sanderbeck et al. 2016)

$$\frac{dT}{dt} = -2HT + \frac{2T}{3\Delta} \frac{d\Delta}{dt} - \frac{T}{n_{\text{tot}}} \frac{dn_{\text{tot}}}{dt} + \frac{2}{3k_B n_{\text{tot}}} \frac{dQ}{dt},$$

where the first term describes adiabatic cooling due to Hubble expansion, the second term describes adiabatic heating or cooling due to density evolution, and the third term describes heating or cooling due to energy equipartition between different species of particles where $n_{\text{tot}}$ is the total number density of baryons (atoms, ions, and electrons). The final term folds all additional heating and cooling processes into $dQ/dt$; in this work, we include photoionization heating due to the H I and He I ionizing backgrounds, for which we assume a power law $J_\nu \propto \nu^{-1.5}$ from 1 to 4 Ryd and zero intensity above 4 Ryd consistent with the pre-He II reionization universe, recombination cooling, collisional ionization cooling, collisional excitation cooling from H I line emission, free–free emission, and inverse Compton cooling off of the CMB. For simplicity, we follow Upton Sanderbeck et al. (2016) and assume a Zel’dovich pancake model for the density evolution of gas elements, $\Delta (a) = [1 - \lambda G(a)]^{-1}$, where $a$ is the scale factor, $G(a)$ is the growth factor, and $\Lambda$ is a constant normalized by reproducing $\Delta$ at $z = 5.7$. In principle, we could compute the Zel’dovich approximated density field for a finely sampled range of redshifts to more consistently compute the density evolution of each cell, but differences in the resulting temperatures would likely be small (McQuinn & Upton Sanderbeck 2016).

We show how the temperature–density relation of gas depends on reionization redshift in Figure 4. Gas at relatively high overdensities ($\Delta > 10$) quickly cools to an equilibrium state, but gas at low density retains substantial excess heat for $\Delta z > 1$ (Trac et al. 2008; Furlanetto & Oh 2009; D’Aloisio et al. 2015). We then apply this temperature evolution model to each cell in the 2048$^3$ semi-numerical cosmological density field through a pre-computed interpolation table of $T(z|z) = 5.7$ as a function of reionization redshift $z_{\text{reion}}$ and $\Delta(z) = 5.7$. The resulting median temperature–density relation is shown by the orange curve in Figure 4, which is similar to the post-reionization state of the IGM found in other works (Trac et al. 2008; Furlanetto & Oh 2009; Lidz & Malloy 2014). The median temperature at mean density $T_0 = 9165$ K is consistent with the measurement inside of quasar proximity zones $T_0 = 7079_{-2370}^{+2370}$ K (95% confidence interval; corrected for local He II photoheating) by Bolton et al. (2012) at $z \sim 6$. In the right panel of Figure 2, we show a $\sim$400 kpc (one cell) slice of the resulting IGM temperature field. Large voids where reionization finished late are hot and nearly isothermal with...
$T \sim 2.5 \times 10^4$ K, while overdense regions which reionized early have relaxed to a power-law temperature–density relation with $T_0 \sim 7500$ K.

2.3. Distribution of Ly$\alpha$ Forest Effective Optical Depth

We compute $\tau_{\text{eff}}$ for many random sightlines through the semi-numerical density field using the fluctuating Gunn–Peterson approximation (FGPA; e.g., Weinberg et al. 1997),

$$\tau_{\text{GP}} \approx 36.1 \kappa \Delta \left(\frac{T}{7500 \text{ K}}\right)^{0.724} \times \left(\frac{\Gamma_{\text{H}1}}{10^{-125} \text{ s}^{-1}}\right)^{-1} \left(\frac{1 + z}{6.7}\right)^{4.5},$$

where $\kappa$ is a re-normalization constant that we tune to match the median observed $\tau_{\text{eff}}$ in the Ly$\alpha$ forest on large scales ($\approx 3.5$, B15). In the fluctuating $\Gamma_{\text{H}1}$ model, we assume that the gas in the IGM follows a power-law temperature–density relation $T = T_0 \Delta^{-\gamma}$ (Hui & Gnedin 1997) with $T_0 = 7500$ K and $\gamma = 1.5$, consistent with the early reionization heating curve in Figure 4. In the residual temperature fluctuations model, we assume a uniform ionizing background with $\Gamma_{\text{H}1} = 3 \times 10^{-13}$ s$^{-1}$. We additionally compute skewers assuming constant $\Gamma_{\text{H}1} = 3 \times 10^{-13}$ s$^{-1}$ and $T = (7500 \text{ K}) \Delta^{0.5}$ to represent the expected $\tau_{\text{eff}}$ fluctuations from the density field alone; this is similar to the typical state of hydrodynamical simulations at $z = 5.7$ which do not include impulsive models for heating during reionization (e.g., Puchwein et al. 2015; Ohorbe et al. 2017). While this simple model for the Ly$\alpha$ forest is unable to produce realistic transmission profiles for individual spectra, the distribution of $\tau_{\text{eff}}$ measured on large scales and how the distribution changes due to $\Gamma_{\text{H}1}$ fluctuations is similar to hydrodynamical simulations (D’Aloisio et al. 2018).

To match the observed median $\tau_{\text{eff}} \sim 3.5$ at $z \sim 5.7$, we require $\kappa = 0.14, 0.31$ for the ionizing background and temperature fluctuations models, respectively. The non-unity value of the constant $\kappa$ mostly reflects our neglect of peculiar velocities and thermal broadening in the calculation of $\tau_{\text{eff}}$ from Equation (2), but also includes more subtle effects such as the limited spatial resolution of our semi-numerical density field. The large difference between the two $\kappa$ values reflects the fact that, in the temperature fluctuations model, low-density gas responsible for Ly$\alpha$ transmission (Oh & Furlanetto 2005) has a much higher typical temperature.

In the top panel of Figure 5, we show the resulting cumulative distribution of $\tau_{\text{eff}}$ on 50 Mpc/h scales for the uniform, fluctuating $\Gamma_{\text{H}1}$, and fluctuating $T_{\text{IGM}}$ models, as well as a model where we include both $\Gamma_{\text{H}1}$ and $T_{\text{IGM}}$ fluctuations. Both fluctuating models broaden the $\tau_{\text{eff}}$ distribution relative to the uniform model, and more closely match a compilation of 31 measurements of $\tau_{\text{eff}}$ with central redshifts between $5.6 < z < 5.8$ from Fan et al. (2006) and B15. When the two fluctuating models are combined, they largely cancel out, reflecting the opposing nature of the environments in which the $\Gamma_{\text{H}1}$ and $T_{\text{IGM}}$ fluctuations increase or decrease $\tau_{\text{eff}}$. In the lower panel of Figure 5, we focus on the high-$\tau_{\text{eff}}$ tail of the distribution, where the differences between the models themselves and with the data are the most pronounced. The

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11 We note that a handful of the data points in this cumulative distribution actually represent 2σ lower limits to $\tau_{\text{eff}}$, most importantly the two measurements at $\tau_{\text{eff}} \sim 7$ in the giant GP trough of ULAS J0148+0600 from B15.
fluctuating ionizing background model shows an extended tail at $\tau_{\text{eff}} \gtrsim 6$ while the temperature fluctuations model falls more rapidly, but at the current sensitivity of the limits of the deepest GP trough in ULAS J0148+0600 (and given the current number of measurements), the two models are largely indistinguishable. This similarity is in qualitative agreement with D’Aloisio et al. (2018), who found that the modifications to the Ly$\alpha$ forest power spectrum on large scales due to fluctuations in $\Gamma_{\text{HI}}$ and $T_{\text{IGM}}$ were roughly equivalent.

Clearly, the distribution of $\tau_{\text{eff}}$ in the Ly$\alpha$ forest is unable to distinguish between the two scenarios for fluctuations that we have considered. One potential avenue for breaking this degeneracy is the difference in the physical nature of GP troughs implied by the models, as we discuss in the following section.

### 3. Relationship between Ly$\alpha$ Forest Opacity and Galaxy Populations

The two models for post-reionization $\tau_{\text{eff}}$ fluctuations that we consider, ionizing background fluctuations and residual temperature fluctuations, make opposite predictions for the nature of GP troughs. If GP troughs are due to ionizing background fluctuations (as in DF16), they arise in large-scale voids that are far away from sources of ionizing photons and exhibit a short mean free path. If GP troughs are instead the result of residual temperature fluctuations (as in D’Aloisio et al. 2015), they arise in large-scale overdense regions that reionized at early times and have had time to cool. In Figure 6, we show maps of the 50 Mpc/$h$-scale $\tau_{\text{eff}}$ centered on the slice shown in Figure 2—compare to the projected density field in the left panel of Figure 1.

While the 100 Mpc/$h$ over- or under-density associated with these regions should be numerically small due to the homogeneity of the universe on such large scales, galaxies at high redshift are highly biased tracers of the density field (Overzier et al. 2009). Thus, in principle, the local galaxy population of GP troughs could favor one model over the other.

Our semi-numerical simulation is well suited to predicting the strength of the correlation between Ly$\alpha$ forest opacity and the co-spatial galaxy population on these large scales. As discussed in Section 2.1, we have abundance matched the halos in our simulation to the observed UV luminosity function of $z \sim 6$ galaxies (Bouwens et al. 2015), so the UV luminosity function of the galaxies in our simulation matches the observations by construction. In Figure 7, we show a close-up on a (100 Mpc/$h$)$^2$ section of the $\tau_{\text{eff}}$ field with overlaid $M_{\text{UV}} < -20$ galaxies, demonstrating a strong spatial relationship between high-$\tau_{\text{eff}}$ regions and bright galaxies which reverses between the $\Gamma_{\text{HI}}$ and $T_{\text{IGM}}$ fluctuations models. To investigate the statistical nature of this relationship, we have computed 1,000,000 randomly oriented lines of sight through both of our fiducial Ly$\alpha$ opacity simulations, described in the previous section, and counted the number of galaxies co-spatial with the Ly$\alpha$ forest region (i.e., within the redshift range of the measured $\tau_{\text{eff}}$) as a function of transverse distance from the sightline and $M_{\text{UV}}$.

In Figure 8, we show the correlation between the number of bright ($M_{\text{UV}} < -21$) galaxies within a transverse separation of 10 arcmin ($\sim 18$ Mpc/$h$) and $\tau_{\text{eff}}$ on 110 Mpc/$h$ scales for our two fluctuations models. The solid lines represent the median number of galaxies at each $\tau_{\text{eff}}$, while the shaded region shows the 16–84th percentiles of the galaxy count distribution. The two models exhibit the trends predicted above: high $\tau_{\text{eff}}$ corresponds to relatively low- or high-density regions, and the strong difference in galaxy counts at $\tau_{\text{eff}} \gtrsim 6$ reflects the large bias of their host halos. In Figure 9, we show a similar test, but for $\tau_{\text{eff}}$ and galaxy counts measured on 50 Mpc/$h$ scales. The trends are weaker because the smaller spatial scale probes less extreme outliers at fixed $\tau_{\text{eff}}$ and the scatter in galaxy counts is higher.

We explore the radial dependence of these correlations in Figure 10 for 110 Mpc/$h$ sightlines with $\tau_{\text{eff}} > 6.5$, showing the surface density of $M_{\text{UV}} < -21$ galaxies as a function of separation on the sky. The correlation between galaxy counts and $\tau_{\text{eff}}$ decreases with distance from the Ly$\alpha$ forest sightline, but is still non-negligible out to separations of $\gtrsim 20$ arcmin ($\gtrsim 36$ Mpc/$h$).

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**Figure 6.** 50 Mpc/$h$-projected Ly$\alpha$ forest $\tau_{\text{eff}}$ for the fluctuating ionizing background (left) and residual temperature fluctuations (right) models, centered on the slice shown in Figure 2. The regions corresponding to low and high $\tau_{\text{eff}}$ correspond to high- and low-density regions, respectively, for the fluctuating ionizing background model, but the opposite is true for the residual temperature fluctuations model.
In practice, counting \( z \sim 5.7 \) galaxies in a large area of the sky presents an observational challenge. While surveys searching for bright high-redshift galaxies using broadband color selection are relatively inexpensive, the precision of photometric redshifts is limited to scales comparable to the window over which \( \tau_{\text{eff}} \) is measured. In Figure 11 we show the effect of a photometric redshift uncertainty \( \sigma_z = 0.25 \) on the correlation between galaxies and \( \tau_{\text{eff}} \). Even for this relatively modest photometric redshift uncertainty \( (\sigma_z/(1+z) \sim 4\%) \), the difference between the two models as compared with

![Projected \( \tau_{\text{eff}} \) [50 Mpc/h] and M_{UV}](image)

**Figure 7.** Zoomed-in portion (100 Mpc/h on a side) of the 50 Mpc/h-projected Ly\( \alpha \) forest \( \tau_{\text{eff}} \) for the fluctuating ionizing background (left) and residual temperature fluctuations (right) models with overlaid \( M_{\text{UV}} < -20 \) galaxies (dots) color and size coded by absolute magnitude. The corresponding region in Figure 6 is centered on (500, 370) Mpc/h. The dashed circles correspond to 10 arcmin radius patches of sky centered on a high \( \tau_{\text{eff}} \) sightline in each model.

![Fluctuating \( \Gamma_{\text{HI}} \) and Fluctuating \( T_{\text{IGM}} \)](image)

**Figure 8.** Relationship between the number of \( M_{\text{UV}} < -21 \) galaxies within a transverse sky separation of 10 arcmin and 110 Mpc/h Ly\( \alpha \) forest effective optical depth for the fluctuating ionizing background model (red) and residual temperature fluctuations model (blue). The vertical dashed line corresponds to the \( \tau_{\text{eff}} \) lower limit of the J0148+0600 GP trough. At high (and low) \( \tau_{\text{eff}} \), the distributions of galaxy counts are highly distinct.

![Fluctuating \( \Gamma_{\text{HI}} \) and Fluctuating \( T_{\text{IGM}} \)](image)

**Figure 9.** Same as Figure 8, but for \( \tau_{\text{eff}} \) and galaxy counts measured on 50 Mpc/h scales.

Figure 8 is greatly reduced due to galaxies scattering into (and out of) the target redshift range where \( \tau_{\text{eff}} \) was measured. Thus, expensive spectroscopic followup would be required to accurately count galaxies associated with the target region of the Ly\( \alpha \) forest.

### 4. Predictions for Ly\( \alpha \) Emitters in the ULAS J0148+0600 GP Trough Environment

A relatively cheap alternative to spectroscopic galaxy surveys is narrowband color selection of Ly\( \alpha \)-emitting galaxies (also known as Ly\( \alpha \) emitters, or LAEs). Fortuitously, Ly\( \alpha \)
To estimate the ability of LAEs to constrain the physical nature of the giant trough, we must associate the dark-matter halos in our semi-numerical simulation to Ly$\alpha$ line luminosities. We have decided to follow a simple empirical approach using the relation between $M_{\text{UV}}$ and the rest-frame equivalent width (REW) of Ly$\alpha$ from (Dijkstra & Wyithe 2012, henceforth DW12). In brief, the Ly$\alpha$ REW of each galaxy is drawn from an exponential distribution,

$$P(\text{REW}|M_{\text{UV}}) \propto \exp\left[-\frac{\text{REW}}{\text{REW}(M_{\text{UV}})}\right],$$

where the scale length is a function of $M_{\text{UV}}$: REW$_c$ = (22 Å) + (6 Å) × ($M_{\text{UV}}$ + 21.9). The distribution includes galaxies with negative REW (i.e., they show Ly$\alpha$ in absorption), and is defined to be zero below REW$_{\text{min}}$ = $-20$ Å for $M_{\text{UV}}$ $< -21.5$, REW$_{\text{min}}$ = $-20 + 6(M_{\text{UV}} + 21.5)^2$ Å for $-19.0 < M_{\text{UV}} < -21.5$, and REW$_{\text{min}}$ = $-5$ Å for $M_{\text{UV}} > -19$. DW12 showed that this distribution was a good fit to the measured distribution of spectroscopically measured Ly$\alpha$ REW for Lyman-break galaxies (LBGs) at $z = 3$–7 (Shapley et al. 2003; Stark et al. 2010).

We select LAEs from the galaxies in our simulation as follows. The Ly$\alpha$ forest is assumed to cover a redshift range 5.52 $< z < 5.88$, and we assigned a redshift $z_{\text{gal}}$ to each associated galaxy based on its location along the line of sight. We compute the i-band and NB816 magnitudes for each galaxy assuming a power-law UV continuum $F_{\nu} \propto \nu^{-\alpha}$ plus the EW of its Ly$\alpha$ line at $z = z_{\text{gal}}$ and evolving IGM attenuation redward of Ly$\alpha$ from the $\tau_{\text{eff}}(z)$ measured by Fan et al. (2006). We then select galaxies as LAEs if $m_{\text{NB816}} < 26$ and i-NB816 $< 1.2$, similar to the sensitivity and criterion of Ouchi et al. (2008), where the limiting narrowband magnitude is achievable with less than one night of exposure time with HSC. Direct application of the distribution from DW12 to the measured galaxy UV luminosity function, however, results in ~2 times as many LAEs as actually detected by narrowband surveys (Ouchi et al. 2008). DW12 found that a simple “correction factor” $F = 0.44$ to the LAE luminosity function computed from the distribution of REWs resulted in a very good fit to observations. We follow this correction in spirit by randomly throwing out 56% of our simulated galaxies that would be selected as LAEs so that we reproduce the observed density of LAEs on the sky. While this is certainly an ad hoc correction, we confirm that, as expected, our simulated LAE population matches the Ly$\alpha$ luminosity function from Ouchi et al. (2008), and that the distributions of LAE counts are robust to changes in the random seed.

Figure 12 shows that the relationship between $\tau_{\text{eff}}$ and the underlying galaxy population (Figure 7) is preserved when LAEs are selected. In Figure 13, we show the analog of Figure 8 for LAEs within 10 arcmin of the Ly$\alpha$ forest sightline. The “signal” in LAE counts tends to be weaker than for the ideal case of a clean spectroscopic galaxy sample for two reasons: first, LAEs tend to lie in less-massive (less-biased) halos, and second, LAEs are only selected in a narrow ~30 Mpc/h window at the center of the sightline where the Ly$\alpha$ line falls into the NB816 filter. The latter fact means that probing giant GP troughs much larger than the size of the Ly$\alpha$ forest region may not matter, and indeed, in Figure 14 we show that the comparison between LAE counts and $\tau_{\text{eff}}$ on 50 Mpc/h scales is nearly identical. Despite the weaker distinction in LAE counts at the tails of the $\tau_{\text{eff}}$ distribution compared to the
spectroscopically complete LBG case, the difference between our two models is quite stark, and should be detectable. We show the cumulative distributions (CDF) of mock LAEs measurements for the two models in Figure 15, demonstrating that the distributions are moderately distinct. To quantify the ability of one measurement to distinguish between the two models, and to find the optimally sized region for comparison, we ask the question: if Model A is true, how likely is it that we rule out Model B at 95% confidence? To estimate this, we use the CDFs of LAE from both models. Specifically, we compute CDF(Σ_{LAE} | fluct. T_{IGM}) with Σ_{LAE} corresponding to CDF(Σ_{LAE} | fluct. T_{IGM}) = 0.05, and CDF(Σ_{LAE} | fluct. \Gamma_{HI}) with Σ_{LAE} corresponding to CDF(Σ_{LAE} | fluct. \Gamma_{HI}) = 0.95.

In Figure 16, we show the resulting probabilities of a single observation of LAEs (m_{NB816} < 26 in a field with τ_{eff} > 6.5) favoring one model over the other at 95% confidence as a function of target sky area. Red and blue curves correspond to the fluctuating T_{IGM} and \Gamma_{HI} models as the “truth,” respectively. The dashed curves assume that we know the background density of LAEs perfectly, while the solid curves perform a differential measurement versus the outer annulus of a HSC field of view (i.e., using the CDFs of Σ_{LAE,target}/Σ_{LAE,field}). In general, a single measurement of LAEs within a radius of 6–12 arcmin has a fairly high probability (∼90%) of preferring the true model over the alternative. The drop-off on scales <10 arcmin is due to the strong signal near the quasar line of sight.

Figure 12. Similar to Figure 7, but with overlaid m_{NB816} < 26 LAEs (dots), color- and size coded by apparent NB816 UV magnitude. Note that the LAEs shown here often do not directly correspond to galaxies shown in Figure 7 because their UV magnitude can be fainter than M_{UV} = −20, thus they were not shown.

Figure 13. Relationship between the number of m_{NB816} < 26 LAEs within a transverse sky separation of 10 arcmin and 110 Mpc/h Ly\alpha forest effective optical depth for the fluctuating background model (red) and residual temperature fluctuations model (blue). The vertical dashed line corresponds to the τ_{eff} lower limit of the J0148+0600 GP trough.

Figure 14. Same as Figure 13, but for τ_{eff} measured on 50 Mpc/h scales.

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should suppress the model, they are overdense, while in the distribution for all \( t_{\text{eff}} \) target radii of 14, 10, and 6 arcmin, respectively. The dotted curves show the statistical approach that uses the full radial number density farther from the line of sight: we leave a more sophisticated being washed out by averaging with more normal regions.

**Figure 15.** Cumulative distributions of \( \Sigma_{\text{LAE}} \) for the fluctuating \( T_{\text{HI}} \) (red) and \( T_{\text{IGM}} \) (blue) models in high \( t_{\text{eff}} \) fields. The top, middle, and bottom panels show target radii of 14, 10, and 6 arcmin, respectively. The dotted curves show the distribution for all \( t_{\text{eff}} \), i.e., the expected distribution of random fields.

being washed out by averaging with more normal regions farther from the line of sight: we leave a more sophisticated statistical approach that uses the full radial number density profile to future work. The dotted curves show the probability that the region can be distinguished from a random patch of sky (with the same area) at 95% confidence. This probability is significantly lower, only \( \sim 30\% - 40\% \). This relatively low probability is due to the large cosmic variance of LAEs in our model, in qualitative agreement with the variations between different fields observed with Subaru/Suprime-Cam by Ouchi et al. (2008), which limits the statistical significance of any excess or deficit of LAEs relative to the field.

**5. Discussion and Conclusion**

The \( \sim 110 \text{ Mpc}/h \) GP trough observed by B15 requires a strong, large-scale difference in the temperature of low-density gas or the strength of the ionizing background. While large-scale overdense regions are likely to be cooler than average because they were reionized early (D’Aloisio et al. 2015), large-scale voids are likely to have a weaker ionizing background (DF16). We have shown that determining whether giant GP troughs are overdense or underdense from large-scale Ly\( \alpha \) forest statistics alone is unlikely, but the corresponding large-scale density fluctuation should lead to a similarly large-scale excess or deficit of galaxies in the surrounding field. While a full spectroscopic inventory of bright LBGs within \( \sim 10 \) arcmin should show a very strong signal, the outcome of less expensive observations of LBGs with photometric redshifts or narrowband-selected LAEs is more subtle. Nevertheless, because the two IGM models we consider make opposing predictions, it appears very likely that a single measurement of LAEs in the ULAS J0148+0600 field will be able to distinguish between the models.

In our predictions for LAEs, we have neglected the potential impact of a fluctuating ionizing background on the escape of Ly\( \alpha \) photons from their local environments. As first shown by Bolton & Haehnelt (2013) and confirmed by others (Choudhury et al. 2015; Mesinger et al. 2015; Kakichi et al. 2016), self-shielded neutral gas in regions with low \( T_{\text{HI}} \) should suppress the observability of LAEs. That is, the weak ionizing background required to produce a giant GP trough may act to suppress the number of LAEs even further than the large-scale void environment, although the strength of this effect depends on the model for escape of Ly\( \alpha \) emission from the galaxies themselves. If the fluctuating \( T_{\text{HI}} \) model is correct, this effect should strengthen the signal (in LAEs) relative to our predictions. In contrast, \( T_{\text{IGM}} \) fluctuations are unlikely to have much of an effect because the thermal state of moderately overdense gas capable of self-shielding is relatively insensitive to reionization heating, as shown by the curves in Figure 4 at \( \Delta \gtrsim 10 \).

While large-scale Ly\( \alpha \) forest transmission measurements are similar between the two IGM models, it is possible that smaller-scale transmission statistics and/or higher-order Lyman-series lines would be more constraining (e.g., Gnedin et al. 2017; Davies et al. 2018). Due to their smaller oscillator strengths, transmission in the higher-order Lyman-series forests is sensitive to gas at higher densities than the Ly\( \alpha \) forest (Oh & Furlanetto 2005), so they are less likely to be fully saturated (cf. the \( \tau_{\text{eff}} = 5.17 \pm 0.05 \) measured in the Ly\( \beta \) forest of the giant GP trough of ULAS J0148+0600). The two models also make predictions for the nature of regions with excess transmission; in the fluctuating \( T_{\text{HI}} \) model, they are overdense, while in the fluctuating \( T_{\text{IGM}} \) model they are hot, underdense environments. The discovery of a sightline with extraordinarily low \( \tau_{\text{eff}} \) at
predicted to exist in the tail of both models we consider, would allow for a definitive test of our hypotheses, but no such regions have yet been identified. High-resolution spectroscopy of regions with strong transmission spikes may be able to distinguish between the two scenarios by measuring something akin to the curvature statistic (Becker et al. 2011a) or wavelet amplitudes (Lidz & Malloy 2014). Another possible avenue of investigation is whether high-redshift low-ionization absorption systems (Becker et al. 2011b), thought to be associated with low-mass galaxies (Finlator et al. 2013), are correlated with \( \tau_{\text{eff}} \). However, the cross-section of such gas around halos is likely also dependent on the strength of the ionizing background and properties of galactic feedback (Keating et al. 2014, 2016), so any such correlations would be challenging to interpret.

Whenever model is correct (if either) will have profound implications for our knowledge of the epoch of reionization. If post-reionization ionizing background fluctuations are strong, then models of the reionization process will have to contend with the effects of a short, spatially varying mean free path which manifest on extremely large scales. If post-reionization temperature fluctuations are strong, then reionization must have been an extended process, and the required amount of heat injection places constraints on the spectra of sources of ionizing photons. Also important is that the alternative model is ruled out due to the strength of the effect and their tendency to cancel each other out (see the orange curve in Figure 5), i.e., either ionizing background or temperature fluctuations must be weak, requiring a long mean free path of ionizing photons or a rapid/low heat input by reionization, respectively. In the future, one could imagine populating Figure 8 and/or Figure 13 with measurements of LBGs and/or LAEs in the foreground of several \( z \gtrsim 6 \) quasars, which should show either a positive or negative trend if either of the models we consider is valid. If no correlation between \( \text{Ly}_\alpha \) opacity and galaxy density is seen, then other factors (e.g., Chardin et al. 2015) may need to be considered.

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