Using a 3.19 fb$^{-1}$ data sample collected at the $\sqrt{s} = 4.178$ GeV with the BESIII detector, we search for the rare decay $D_{s}^{+} \rightarrow p\pi^{+}\nu_{\mu}$. No significant signal is observed, and an upper limit of $B(D_{s}^{+} \rightarrow p\pi^{+}\nu_{\mu}) < 2.0 \times 10^{-4}$ is set at the 90% confidence level. This measurement is useful input in understanding the baryonic transition of $D_{s}^{+}$ mesons.

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I. INTRODUCTION

In the charm sector, probing the transition between charm meson and baryon pairs is still largely an unexplored territory. Phase-space constraints dictate that...
only the $D_s^+$ meson can decay in such a manner. Until now, only one baryonic mode, $D_s^+ \to p\bar{n}$, has been observed. It was first seen by the CLEO Collaboration, with a branching fraction of \((1.30 \pm 0.4) \times 10^{-3}\) \cite{3}, and subsequently confirmed by BESIII \cite{5}. This mode is expected to be suppressed by chiral symmetry, and predictions for its decay rate are several orders of magnitude below the observed value \cite{3}, motivating the study of other baryonic channels. A promising candidate is the semileptonic decay mode $D_s^+ \to p\bar{p}e^+\nu_e$, for which theoretical calculations are expected to be more robust. Recently, H. Y. Cheng and X. W. Kang \cite{6} predicted a small branching fraction, $\mathcal{B}(D_s^+ \to p\bar{p}e^+\nu_e) \sim 10^{-8}$. Even in this case, however, there are significant uncertainties on the prediction, associated with the challenge of calculating the hadronic form factor. Experimental input is therefore needed to help illuminate this poorly understood class of charm decays.

An additional motivation for searching for this decay is that the final state provides an ideal laboratory to study near-threshold enhancement phenomenon. This behavior was initially observed in the radiative process $J/\psi \to \gamma p\bar{p}$ by BESIII \cite{5} and confirmed by CLEO \cite{8} and BESIII \cite{5}, but not yet observed in other processes \cite{9,10}. A very attractive feature of searching for this phenomenon in $D_s^+ \to p\bar{p}e^+\nu_e$ decays is that the $p\bar{p}$ system is produced close to mass threshold.

With the strong interaction dynamics described by a form factor $f_+(q^2)$, and in the limit of zero electron mass, the differential rate for the $D_s^+ \to p\bar{p}e^+\nu_e$ decay is given by

$$d\Gamma(D_s^+ \to X e^+\nu_e) = \frac{G_F^2 |V_{cs}|^2}{24\pi^3} p_X^3 |f_+(q^2)|^2,$$  \hspace{1cm} (1)

where $G_F$ is the Fermi constant, $V_{cs}$ is the Cabibbo-Kobayashi-Maskawa (CKM) matrix element, the $X$ represents the $p\bar{p}$ system, which is assumed to form a $^3S_0$ state, $p_X$ is the momentum of $p\bar{p}$ system in the rest frame of the $D_s^+$ meson, and $q$ is the transition momentum between $X$ and $D_s^+$. The form factor $f_+(q^2)$ is described by the well known ISGW2 model \cite{11},

$$f_+(q^2) = f_+(q^2_{\text{max}}) \left( 1 + \frac{r^2}{12} (q^2_{\text{max}} - q^2) \right)^{-1},$$  \hspace{1cm} (2)

where $r$ is the effective radius of the $D_s^+$ meson, and $q^2_{\text{max}}$ is the kinematic limit of $q^2$.

In this article, we report a search for the decay $D_s^+ \to p\bar{p}e^+\nu_e$ using a 3.19 fb\(^{-1}\) data set collected at $\sqrt{s} = 4.178$ GeV with the BESIII detector operating at the BEPCII collider.

II. BESIII DETECTOR AND MONTE CARLO SIMULATION

The BESIII detector is a magnetic spectrometer \cite{12} located at the Beijing Electron Position Col-lider (BEPCHII) \cite{13}. The cylindrical core of the BESIII detector consists of a helium-based multilayer drift chamber (MDC), a plastic scintillator time-of-flight system (TOF), and a CsI (TI) electromagnetic calorimeter (EMC), which are all enclosed in a superconducting solenoidal magnet providing a 1.0 T magnetic field. The solenoid is supported by an octagonal flux-return yoke interleaved with steel. The acceptance of charged particles and photons is 93\% over the 4\pi solid angle. The charged-particle momentum resolution at 1 GeV/c is 0.5\%, and the $dE/dx$ resolution is 6\% for the electrons from Bhabha scattering. The EMC measures photon energies with a resolution of 2.5\% (5\%) at 1 GeV in the barrel (end-cap) region. The time resolution of the TOF barrel part is 68 ps. The end-cap TOF system was upgraded in 2015 with multi-gap resistive plate chamber technology, providing a time resolution of 60 ps \cite{14,15}.

Simulated events are generated with a GEANT4-based \cite{16} software package using a detailed description of the detector geometry and of the particle interactions in the detector material. A sample of inclusive Monte Carlo (MC) simulation is produced at $\sqrt{s} = 4.178$ GeV. This sample includes all known open-charm decay processes and the $c\bar{c}$ resonances, $J/\psi$, $\psi(3686)$ and $\psi(3770)$ via the initial state radiation (ISR). Additionally, the continuum process ($e^+e^- \to q\bar{q}$, $q = u, d,$ and $s$), Bhabha scattering, $\mu^+\mu^-$, $\tau^+\tau^-$, as well as two-photon process are included. The open charm processes are generated using CONEXC \cite{17} and their subsequent decays are modeled by EVTGEN \cite{18} with the known branching fractions from the Particle Data Group \cite{19}, and the remaining unknown decay modes of the narrow $c\bar{c}$ resonances are generated using the modified LUND model \cite{20}. The signal model is described by Eq. \eqref{eqn:1}. We assume that the $p\bar{p}$ S-wave system dominates in the decay and adopt a non-resonance S-wave to describe the $p\bar{p}$ system (when assigning the systematic uncertainties we also consider the possibility of a resonance contributing to the decay).

III. ANALYSIS METHOD

Throughout the paper, charge-conjugate modes are implicitly implied, unless otherwise noted. The $D_s^+D_s^{+\mp}$ pairs are produced at a center-of-mass energy of 4.178 GeV. The double tag (DT) method is employed to perform a measurement of the absolute branching fraction. We first select “single tag” (ST) events in which either a $D_s^-$ or $D_s^+$ meson is fully reconstructed. Then the $D_s^+$ decay of the interest is searched for in the remainder of each event, namely, in DT events where both the $D_s^+$ and $D_s^-$ are fully reconstructed, regardless of the $\gamma$ or $n^0$ emitted from $D_s^{\pm}$ meson. The absolute branching fraction for the $D_s^+$ meson decay is calculated for each tag mode $\alpha$, and is given by

$$B_{\text{sig}}^\alpha = \frac{N_{\text{ST}}^\alpha}{N_{\text{ST}}^{\alpha DT}/\gamma_{\text{ST}}},$$  \hspace{1cm} (3)
where $N_{\alpha}^{ST}$ and $N_{\alpha}^{DT}$ are the yields of ST events and DT events, respectively, and $\epsilon_{\alpha}^{ST}$ and $\epsilon_{\alpha}^{DT}$ are the ST and DT efficiencies for the tag mode $\alpha$.

A. ST Analysis

All charged tracks must have a polar angle ($\theta$) within $|\cos \theta| < 0.93$, where $\theta$ is measured with respect to the direction of the beam. Furthermore, all charged tracks, apart from those from $K_S^0$ candidates, are required to point back to the interaction point (IP). This is achieved by imposing $V_r < 1$ cm and $|V_z| < 10$ cm, where $V_r$ and $|V_z|$ are the distances of the closest approach to the IP in the transverse plane and along the positron beam direction, respectively. The information from the $dE/dx$ and TOF measurements are combined to evaluate the particle identification (PID) probability ($\mathcal{L}$). A charged track is assigned to be a kaon (pion) candidate if it satisfies $\mathcal{L}_{\pi} < \mathcal{L}_{\pi(K)}$. Candidate $K_S^0$ mesons are formed from two oppositely charged tracks satisfying $|V_z| < 20$ cm and $|\cos \theta| < 0.93$, which are assumed to be pions without the imposition of further PID requirements. These two tracks are constrained to have a common vertex and the invariant mass of the pair is required to lie within $(0.487, 0.511)$ GeV/$c^2$. The decay length of the $K_S^0$ candidates is required to be larger than twice the uncertainty of the decay length.

The $D_s^-$ single-tag candidates are reconstructed in the three tag modes, $K^+K^-\pi^-$, $K_S^0K^-$ and $K_S^0K^+\pi^-\pi^-$, which all have high signal-to-noise ratios and yield the highest sensitivity, according to studies performed on the inclusive MC sample.

To suppress the background involving $D^* \to D\pi$ decays, the momenta of pions from the $D_s^-$ decay are required to be greater than 0.1 GeV/$c$. The recoil mass evaluated against the $D_s^-$ candidate, $M_{\text{recoil}}(D_s^-) = \sqrt{(\sqrt{s} - E_{D_s^-})^2 - |\vec{p}_{D_s^-}|^2}$, is used to reject background from non-$D_s^0 D_s^{*+}$ processes with the requirement that

$$2.06 < M_{\text{recoil}}(D_s^-) < 2.18 \text{ GeV}/c^2.$$

If there are several $D_s^-$ candidates in the event, only that one with recoil mass closest to the $D_s^{*+}$ nominal mass is retained.

An unbinned maximum-likelihood fit is performed on the $M_{D_s^-}$ spectrum of each of the three selected ST tag modes, as shown in Fig. 1. In the fit, the signal shape is taken from the distribution found in MC simulation, using the kernel-estimation method [21] provided as a RooKeysPdf class in ROOT [22], convolved with a Gaussian function. The non-peaking background is described by a second- or third-order Chebyshev polynomial. The small peaking contribution seen in the $D_s^-\to K_S^0\pi^-$ mode is from $D^-\to K_S^0\pi^-$ decays and its shape is taken from MC simulation, with the absolute normalization determined from the fit.

All the selected $D_s^-$ candidates are retained for further analysis. The resultant yields, $N_{\alpha}^{ST}$, and the corresponding selection efficiencies $\epsilon_{\alpha}^{ST}$, as determined from the simulation, are summarized in Table 1. The total yield of single tags is $N_{\alpha}^{ST} = 186091 \pm 719$, where the uncertainty is statistical.

![Fig. 1. Fit to the $M_{D_s^-}$ spectrum for each tag mode. The dots with error bars are from the data. The blue solid lines represent the total fit result. The red dashed line and green long and dashed line are the signal shape, and non-peaking background. The pink dotted line in the $K_S^0K^-$ tag mode corresponds to the peak background due to $D^-\to K_S^0\pi^-$.](image)

| Mode                | $N_{\alpha}^{ST}$ | $\epsilon_{\alpha}^{ST}$ (%) | $\epsilon_{\alpha}^{DT}$ (%) |
|---------------------|-------------------|-------------------------------|-------------------------------|
| $K_S^0K^-$          | 31267±261         | 42.32±0.04                    | 8.63±0.07                     |
| $K^+K^-\pi^-$       | 140277±635       | 49.33±0.18                    | 9.62±0.08                     |
| $K_S^0K^+\pi^-\pi^-$| 14547±214        | 21.08±0.07                    | 3.82±0.04                     |
B. DT Analysis

After the reconstruction of the ST $D_s^-$ candidate, there are required to be fewer than four unused charged tracks in the event. We search for proton and electron candidates among these unused tracks. The charged tracks are assigned as proton candidates if they satisfy $L_p > L_K$, and $L_p > L_\pi$.

As shown in Fig. 2(a), the momentum of the electron in the signal decay is typically very low. Consequently, in most decays the electron is not reconstructed in the detector. The presence of the $p\bar{p}$ pair, however, is a sufficiently distinctive signature for such events to be classified as signal, even in the cases when there is no track reconstructed corresponding to the electron. In those cases when a third track is found with lower momentum than the $p$ and $\bar{p}$ candidates, which happens in about 5% of selected events, this track is assigned to be the electron candidate without any PID requirement. Requiring that the momentum of the electron candidate is smaller than 0.09 GeV/c reduces background, whose spectrum is also shown in Fig. 2(b). The missing mass-squared $MM^2 = (\sqrt{s} - E_{tag} - E_{sig})^2 - (\vec{p}_{tag} + \vec{p}_{sig})^2$ is required to be larger than 0 GeV$^2$/c$^4$ to further reduce the background from continuum $q\bar{q}$ production, as shown in Fig. 2(b). Here $E_{tag}$, $\vec{p}_{tag}$ and $E_{sig}$, $\vec{p}_{sig}$ are the total energy and momentum of the tag side and signal side, respectively. As we ignore the momentum of the photon or $\pi^0$ from the $D_s^-$ decay, the signal has a predominantly positive value of $MM^2$ as can be seen in Fig. 2(b).

The DT efficiencies $\epsilon^0_{DT}$ as summarized in Table 1 are determined from simulation and later corrected for the PID differences between data and MC simulation.

An extended unbinned maximum-likelihood fit to the $M_{D_s^-}$ distribution of the tag meson is used to determine the number of DT signal events. For the tag mode $\alpha$, the likelihood value is defined as

$$L^\alpha = \frac{e^{-(N_{sig}^\alpha + N_{bkg}^\alpha)}}{n^\alpha!} \times \prod_{i=1}^{n^\alpha} \left( N_{sig}^\alpha \mathcal{P}^\alpha_{sig}(M_{D_s^-}) + N_{bkg}^\alpha \mathcal{P}^\alpha_{bkg}(M_{D_s^-}) \right),$$

where $n^\alpha = N_{sig}^\alpha + N_{bkg}^\alpha$ is the number of total observed DT events. $N_{sig}^\alpha$ and $N_{bkg}^\alpha$ denote the fitted yields for signal and backgrounds, respectively, and $\mathcal{P}_{sig}^\alpha$ and $\mathcal{P}_{bkg}^\alpha$ are the corresponding probability density functions (PDF) in the fit. The PDF distributions are taken from simulation, with the inclusive MC sample being used to represent the background.

A simultaneous fit to the $M_{D_s^-}$ spectra from the three tag modes is performed with the combined likelihood

$$L^{\text{com}} = \prod_{\alpha=1}^{3} L^\alpha,$$

sharing the same branching fraction of $D_s^+ \rightarrow p\bar{p}e^+\nu_e$ for each.

The fit results are shown in Fig. 3. The signal yields for the three selected ST modes are determined to be $0.3^{+0.4}_{-0.3}$, $1.4^{+1.8}_{-1.3}$, $0.1 \pm 0.1$, respectively, and the branching fraction is measured to be $B(D_s^+ \rightarrow p\bar{p}e^+\nu_e) = (0.50^{+0.63}_{-0.44}) \times 10^{-4}$ with a significance of 1.2$\sigma$, where the uncertainty is statistical. Since no significant signals are seen, we set an upper limit after taking into account the systematic uncertainties.

IV. SYSTEMATIC UNCERTAINTIES

Possible sources of systematic bias are investigated, and corresponding uncertainties are assigned as discussed below. These uncertainties are listed and added in quadrature in Table 2, apart from that component associated with the fit of the DT yields, which is accounted separately.
Fig. 3. Fits to $M_{D^{-}}$ after DT event selection. The points with error bars are data, and the blue solid lines show the total fit result. The red and green dotted lines denote the signal and background shapes, respectively.

A. Fitting ST $M(D_{s}^{+})$ yields

A set of alternative fits is performed, in which the following variations are applied: the background shape is changed from a second- to a third-order Chebyshev polynomial; the signal shape is changed from the MC-simulated shape convolved with a single Gaussian function to the sum of two Gaussian functions; and the fitting range is both increased and decreased by 5 MeV/$c^{2}$. The procedures are performed both on inclusive MC and data, and the overall sum in quadrature of the observed differences in the efficiency corrected signal yields is taken as the systematic uncertainty associated with fitting the ST $M_{D^{-}}$ yields.

B. Tracking and PID

The uncertainties associated with the knowledge of the tracking and PID efficiencies for the proton and anti-proton are studied with a control sample of $e^{+}e^{-} \rightarrow p\bar{p}\pi^{+}\pi^{-}$ decays. The signal efficiency is re-weighted according to the momentum distributions of the proton and anti-proton. The uncertainties associated with the tracking and PID efficiencies are assigned to be 2.9% and 2.2%, respectively.

C. MM$^{2}$ requirement

The systematic uncertainty from the MM$^{2}$ requirement is associated with the knowledge of the detector resolution. To estimate this uncertainty a control sample is selected, which has the same tag modes for the $D_{s}^{-}$ as in the nominal analysis, and where the other meson is reconstructed in the mode $D_{s}^{+} \rightarrow K^{+}K^{-}\pi^{+}$, with the pion then removed and treated as a missing particle. The MM$^{2}$ resolution is compared between data and MC simulation, and the difference is applied as additional smearing to the signal MC sample. The difference between the selection efficiencies with this treatment and the nominal analysis is assigned as the systematic uncertainty due to the MM$^{2}$ requirement.

D. MC modeling

To estimate the systematic uncertainty due to the possibility of a $p\bar{p}$ bound state, and its assumed mass and width, we simulate and analyze new MC samples that include a resonant system in the decay. We vary the mass of the system from 1.80 to 1.85 GeV/$c^{2}$, and the width from 10 to 100 MeV/$c^{2}$ [5–7]. The largest relative change of the signal efficiency is found to be 18% and is assigned as the uncertainty from MC modeling.

E. Fitting

It is only necessary to consider the uncertainty on the knowledge of the background shape, as that associated with the signal distribution has negligible impact on the result. The background shape is obtained using the kernel estimation method [21] provided as a RooKeysPdf Class in ROOT [22], based on the inclusive MC sample. Unlike the other sources of uncertainties, the background shape affects the likelihood function directly. We vary the smoothing parameter of RooKeysPdf within a reasonable range to obtain alternative background shapes. We adopt the background shape that gives the largest upper limit on the signal branching ratio to assign the value of this component of the systematic uncertainties.
Table 2. The relative systematic uncertainties (in percent).

| Source                  | Uncertainty |
|-------------------------|-------------|
| ST yields               | 0.8         |
| Tracking efficiency     | 2.9         |
| PID efficiency          | 2.2         |
| \(MM^2\) requirement    | 1.0         |
| MC modeling             | 18          |
| Total                   | 19          |

V. RESULT AND SUMMARY

The upper limit (UL) on the branching fraction is set at the 90% confidence level (CL) according to

\[
\frac{\int_0^{UL} L(B) dB}{\int_0^1 L(B) dB} = 0.9. \tag{5}
\]

In order to improve this limit, and approach the predicted branching ratio of Ref. [4], larger data samples are needed, either at BESIII, or at future experiments such as Belle II experiment [24] and super tau-charm factory [25, 26].

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