Semi-supervised t-SNE for Millimeter-wave Wireless Localization

Junquan Deng¹,*, Wei Shi¹, Jian Hu¹, Xianlong Jiao²

¹Sixty-third Research Institute, National University of Defense Technology, China, Emails: jqdeng@nudt.edu.cn
²College of Computer Science, Chongqing University, China, Email: xljiao@cqu.edu.cn

Abstract—We consider the mobile localization problem in future millimeter-wave wireless networks with distributed Base Stations (BSs) based on multi-antenna channel state information (CSI). For this problem, we propose a Semi-supervised t-distributed Stochastic Neighbor Embedding (St-SNE) algorithm to directly embed the high-dimensional CSI samples into the 2D geographical map. We evaluate the performance of St-SNE in a simulated urban outdoor millimeter-wave radio access network. Our results show that St-SNE achieves a mean localization error of 6.8m with only 5% of labeled CSI samples in a 200 x 200 m² area with a ray-tracing channel model. St-SNE does not require accurate synchronization among multiple BSs, and is promising for future large-scale millimeter-wave localization.

Index Terms—Channel-state information (CSI), millimeter-wave, wireless localization, semi-supervised learning, t-SNE

I. INTRODUCTION

The mobile location information of User Equipments (UE) is critical for many smart city applications, including traffic monitoring, asset tracking, autonomous driving, emergency rescue and so forth. Currently, mobile localization heavily depends on global navigation satellite system (GNSS) technologies, but GNSSs are not omnipotent for all kinds of applications and all scenarios. For example, a GNSS may fail to provide reliable position estimates due to signal blockage in dense urban areas. Furthermore, continuous reception and detection of GNSS signals is a major part of battery consumption for many mobile devices. In some applications where a central entity needs to collect location information from massive user devices, GNSS is not adequate as users may refuse to report their GNSS information. Due to these problems, we need to resort to other complementary methods for localization and positioning where GNSSs are not suitable.

Future 5G and beyond radio access networks (RANs) are envisioned to be densely deployed with massive multi-antenna Base Stations (BSs) and high-frequency carrier frequencies, such as millimeter-wave (mmWave), to provide ubiquitous ultra-fast and reliable wireless connections. In addition to communication, the large-scale dense RAN infrastructure, the massive antennas and the wide high-frequency bands can also be leveraged for sensing and localization purposes [1]–[4].

However, current 5G New Radio positioning techniques are based on triangulation with Angle-of-Arrival (AOA) or trilateration with Time-Difference-of-Arrival (TDOA) measurements at multiple BSs, which require accurate calibration and synchronization among RAN elements, and thus incur high deployment and maintenance costs for the operators. Moreover, the performance of these methods degrades in complex multi-path and obstructed environments. Fingerprinting techniques [6]–[8] could be applied for cellular positioning in such challenging propagation environments. However, they require a large amount of dedicated and densely-sampled labeled measurements, so scale poorly to large areas and render automatic operation and maintenance in dynamic environments challenging. As unlabeled samples are easier to be collected, semi-supervised learning methods [9] with both labeled and unlabeled data are promising for automatic large-scale localization. Semi-supervised learning has attracted increasing attention for positioning based on Received Signal Strength Indicator (RSSI) fingerprints [10], [11]. However, research work on utilizing multi-antenna Channel State Information (CSI) [12], [13] for high-precision and seamless localization in a networking environment is still limited.

Recently, channel charting [14], [15] has been proposed to use sporadically collected multi-antenna CSI samples from unknown locations to construct a channel chart that can provide relative position information among UEs. Channel charting exploits the fact that high-dimensional multi-antenna CSI strongly depends on the low-dimensional 2D/3D UE location as a result of physical law of radio propagation. Several works [16]–[18] have dedicated to equip channel charting with absolute positioning capabilities. In [16], a semi-supervised auto-encoder has been proposed to utilize a subset CSI of samples with known spatial locations, as well as mobility side information to locate UEs in a single cell. In [17], Sammon’s mapping (SM) and Siamese neural network are combined in an unified channel charting framework to provide both unsupervised relative localization, and semi-supervised absolute positioning. Unfortunately, in a scenario with challenging non-Line-of-Sight (NLOS) propagation channels, the localization performance of [16], [17] is not satisfying. In addition, these two methods have not considered the more realistic large-scale multi-cell scenario with multiple BSs. For multi-cell localization, a semi-supervised multi-point channel charting (SS-MPCC) framework has been put forward in [18]. In SS-MPCC, multiple distributed BSs collect wireless data...
We consider a typical 5G mmWave cellular network where multiple UEs move in the coverage area of multiple BSs. The UEs send Orthogonal Frequency Division Multiplexing (OFDM) pilot signals to BSs for channel estimation. An estimated multi-antenna channel vector at time $t$ on a sub-carrier with frequency $f$ is modelled as

$$\mathbf{h}_{t,f} = \sum_{k=1}^{K} \alpha_{t,f}^{(k)} \mathbf{s}(\phi_{t}^{(k)}) + \mathbf{e},$$

where $K$ denotes the number of multi-path components, $\phi_{t}^{(k)}$ the direction-of-arrival (DOA) of the $k$th propagation path, and $\alpha_{t,f}^{(k)}$ a random complex gain for the $k$th path. In addition, $\mathbf{e}$ represents the channel estimation error, and $\mathbf{s}(\phi)$ the array steering vector (ASV).

We assume an $M$-antenna uniform linear array is used at a BS, and the ASV is

$$\mathbf{s}(\phi) = [1, e^{j \frac{2\pi}{\lambda} s \sin(\phi)}, \ldots, e^{j (M-1) \frac{2\pi}{\lambda} s \sin(\phi)}]^T,$$

with $\lambda$ the carrier wavelength and $s$ the antenna spacing.

### B. CSI Collection and Dissimilarity Matrix Construction

The channel vector $\mathbf{h}_{t,f}$ itself changes rapidly when the UE moves across multiple wavelengths. In comparison, the multipath DOAs $\{\phi_{t}^{(l)}\}$ and gains $\{\alpha_{t}^{(l)}\}$ change more slowly. We use the frequency-domain covariance $\mathbf{C} = \mathbb{E}_f [\mathbf{h}_{t,f} \mathbf{h}_{t,f}^H]$ as the CSI sample for localization, as it depends on the multipath DOAs and gains, and changes slowly when UE moves.

We assume there are $B$ BSs, they will collect CSI samples from multiple UEs during network operation. There are two types of CSI samples, with or without position labels. The first type has the corresponding UE position information which can be gathered in a dedicated site survey or reported by UEs with GNSS capability, while the second type is collected from UEs which need to be located or tracked. After data collection, we assume there are $L$ labeled CSI samples at BS $b$, denoted by $\mathcal{L}^{(b)} = \{C_1^{(b)}, \ldots, C_L^{(b)}\}$. The corresponding ground-truth location coordinates are $\mathbf{Y} = [y_1, \ldots, y_L]$. The in total $U$ unlabeled samples collected at BS $b$ can be denoted as $\mathcal{U}^{(b)} = \{C_{L+1}^{(b)}, \ldots, C_{L+U}^{(b)}\}$. The corresponding unknown locations for the unlabeled samples are denoted by $\hat{\mathbf{Y}} = [y_{L+1}, \ldots, y_{L+U}]$. We assume that multiple BSs can identity the CSI samples coming from a specific UE at a same time interval via UE ID and loose time synchronization. If an UE’s pilot signals are not received by BS $b$ at a time, the corresponding CSI sample $C_i^{(b)}$ is set to zeros. Each BS will utilize a feature extraction function to extract the power angular profile (PAP) of multipath components (MPCs) hidden in the CSI sample and compute the dissimilarities among its collected samples. The CU then fuse the local dissimilarities and channel qualities information reported by BSs to construct a global consistent dissimilarity matrix $\mathbf{D} \in \mathbb{R}^{N \times N}$, with $N = L+U$. The details of the feature extraction, dissimilarity metric and fusion procedures can be found in [18]. The global dissimilarity matrix $\mathbf{D}$ characterizes how similar the uplink radio channel conditions for different UE positions.
III. SEMI-SUPERVISED t-SNE

The t-SNE [19] is an effective dimensional reduction and manifold learning algorithm widely used for visualizing high-dimensional data. This method learns a low-dimensional representation \( \mathbf{Z} = [\mathbf{z}_1, ..., \mathbf{z}_N] \) of the \( N \) data points by minimizing the divergence between two distributions, i.e., a distribution that characterizes pairwise similarities of the input data points, and a distribution that characterizes pairwise similarities of the corresponding low-dimensional points in the representation space. To this end, t-SNE defines a symmetric probability matrix \( \mathbf{P} \) with elements \( \{p_{nm}\}_{n,m=1}^N \) that measures the pairwise similarity between \( n \)th and \( m \)th input data points. Denote \( \{d_{nm}\}_{n,m=1}^N \) the entities of the dissimilarity matrix \( \mathbf{D} \), for \( n \neq m \), we have

\[
p_{nm} = \frac{1}{2}(p_{mn} + p_{nm}) = \frac{1}{2} \left( \sum_{k \neq n} e^{-d_{kn}/2\sigma_k^2} + \sum_{k \neq m} e^{-d_{km}/2\sigma_k^2} \right),
\]

and \( p_{nm} = 0 \) for \( n = m \), with \( p_{mn} \) the conditional probability the \( m \)th point is a neighbor of the \( n \)th point . The bandwidth of the Gaussian kernels \( \sigma_n \) for the \( n \)th data point is set so that \( 2^{-\sum_m p_{mn}} \log_2 p_{mn} \) equals to a given parameter \( k_t \) called perplexity, e.g., using a 1D search method. The perplexity can be interpreted as a measure of the effective number of neighbors taken into account.

In the representation space, a matrix \( \mathbf{Q} \) with element \( \{q_{nm}\}_{n,m=1}^N \) which measures the similarity between \( \mathbf{z}_n \) and \( \mathbf{z}_m \), is computed using a normalized t-distribution kernel by

\[
q_{nm} = \frac{(1 + ||\mathbf{z}_n - \mathbf{z}_m||_2^2)^{-1}}{\sum_{l \neq k} (1 + ||\mathbf{z}_l - \mathbf{z}_k||_2^2)^{-1}}.
\]

The objective of t-SNE is to find a representation by minimizing the Kullback-Leibler (KL) divergence between the two distributions \( \mathbf{P} \) and \( \mathbf{Q} \). The optimization problem is

\[
\begin{align*}
(\text{P}1) \quad & \text{minimize} & f_{t\text{-SNE}}(\mathbf{Z}) = \sum_n \sum_m p_{nm} \log \frac{p_{nm}}{q_{nm}}, \\
\text{subject to} & \sum_{n=1}^N \mathbf{z}_n = 0.
\end{align*}
\]

The objective function \( f_{t\text{-SNE}}(\mathbf{Z}) \) can be minimized by gradient descent. Note that the KL divergence is not convex. Different initializations will possibly end up in different local minima of \( f_{t\text{-SNE}}(\mathbf{Z}) \). Hence, it is useful to try different seeds and choose the result with the lowest KL divergence. t-SNE is computationally expensive, especially for large-scale data sets. Larger perplexities lead to more neighbors and less sensitivity to small-scale structure. By contrast, a lower perplexity focuses on a smaller number of neighbors, and thus ignores more global information favouring the local neighborhood preservation. For a larger data set, larger perplexities are required.

Directly solve problem P1 can not provide a 2D map with estimated UE position information. To equip t-SNE with localization capability, we need to use some position labels to govern the learning process of t-SNE. To this end, we formalize the following semi-supervised t-SNE problem,

\[
\begin{align*}
(\text{P2}) \quad & \text{minimize} & \tilde{f}_{t\text{-SNE}}(\mathbf{Z}) = \sum_n \sum_m p_{nm} \log \frac{p_{nm}}{q_{nm}}, \\
\text{subject to} & \mathbf{z}_i = \mathbf{y}_i, i = \{1, \ldots, L\}.
\end{align*}
\]

As the labeled CSI samples are restricted to be mapped to their corresponding true UE locations, minimizing the cost function would probably lead to an UE position map, and the unknown locations of unlabeled samples can be estimated. As shown in [19], the gradient of the Kullback-Leibler divergence between \( \tilde{\mathbf{P}} \) and \( \tilde{\mathbf{Q}} \) is given by

\[
\frac{df_{t\text{-SNE}}(\mathbf{Z})}{d\mathbf{z}_n} = 4 \sum_m \frac{(p_{nm} - q_{nm})(\mathbf{z}_n - \mathbf{z}_m)}{(1 + ||\mathbf{z}_n - \mathbf{z}_m||_2^2)}.
\]

To solve problem P2, we have devised a gradient descent algorithm as summarized in Algorithm 1. In Algorithm 1, the learning process is controlled by four parameters, the perplexity \( k_t \), iteration number \( T \), learning rate \( \eta \) and momentum \( \alpha \). They will be investigated in Section IV-B. At the end of each iteration, the coordinates of the labeled points in the 2D map are forced to be equal to their position labels, so the learned 2D map would be aligned in the geographical space. The computation complexity of one iteration in Algorithm 1 is \( O(N^2) \) [19], and the overall complexity is \( O(TN^2) \).

\[\text{INPUTS: } \mathbf{D} \in \mathbb{R}^{N \times N}, \{y_1, \ldots, y_L\}, \mathcal{L} = \{1, \ldots, L\}\]

Algorithm 1 The semi-supervised t-SNE algorithm

1: \textbf{Initialize: } \mathbf{Z}(0) = [\mathbf{z}^{(0)}_1, \ldots, \mathbf{z}^{(0)}_N], \mathbf{Z}^{(-1)} = \mathbf{Z}(0), \text{with } \mathbf{Z}^{(0)}_i = \mathbf{y}_i, i \in \mathcal{L}. \\
2: \textbf{Cost function parameter: } k_t \\
3: \textbf{Optimization parameters: } T, \eta \text{ and } \alpha \\
4: \textbf{Initialize: } \mathbf{Z}(0) = [\mathbf{z}^{(0)}_1, \ldots, \mathbf{z}^{(0)}_N], \mathbf{Z}^{(-1)} = \mathbf{Z}(0), \text{with } \mathbf{Z}^{(0)}_i = \mathbf{y}_i, i \in \mathcal{L}. \\
5: \textbf{Initialize: } \mathbf{Z}(0) = [\mathbf{z}^{(0)}_1, \ldots, \mathbf{z}^{(0)}_N], \mathbf{Z}^{(-1)} = \mathbf{Z}(0), \text{with } \mathbf{Z}^{(0)}_i = \mathbf{y}_i, i \in \mathcal{L}. \\
6: \textbf{Update position: } \mathbf{z}_i = \mathbf{y}_i, i \notin \mathcal{L} \text{ and } d_{n,i} \text{ is smallest for all } n \neq i. \\
7: \textbf{Use binary search to determine the kernel sizes } \{\delta_{nm}\}_{n,m=1}^N, \text{ and compute the probability matrix } \mathbf{P} \text{ using } (3). \\
8: \textbf{for } t = 1, \ldots, T \text{ do} \\
9: \quad \textbf{Compute probability matrix } \mathbf{Q} \text{ using } (4) \\
10: \quad \textbf{Compute gradient } \nabla = \{\frac{df_{t\text{-SNE}}(\mathbf{Z})}{d\mathbf{z}_1}, \ldots, \frac{df_{t\text{-SNE}}(\mathbf{Z})}{d\mathbf{z}_N}\} \text{ using } (5) \\
11: \quad \textbf{Update } \mathbf{Z}(t) = \mathbf{Z}(t-1) + \eta \nabla + \alpha (\mathbf{Z}(t-1) - \mathbf{Z}(t-2)) \\
12: \quad \textbf{Set } \mathbf{z}_i(t) = \mathbf{y}_i, i \in \mathcal{L} \\
13: \textbf{end for} \\
14: \textbf{return: } \mathbf{Z}(T) \\
\]

IV. SIMULATION RESULTS

We now demonstrate the efficacy of the proposed St-SNE algorithm for CSI-based localization with a subset of CSI samples with marked positions, investigate the effects of its learning parameters on the performance, and compare it with some other typical CSI-based localization methods.

A. Simulated Scenario and Evaluation Metric

We consider a dense urban outdoor multi-cell mmWave network scenario as depicted in Fig. 2. BSs are below rooftop, and signals will be reflected or blocked by the walls. A ray-tracing channel model is used to generate the multi-path channels. The reflection coefficients are computed based on
TABLE I
BASIC SIMULATION PARAMETERS

| Parameter               | Value     | Parameter               | Value     |
|-------------------------|-----------|-------------------------|-----------|
| Carrier frequency       | 28 GHz    | UE pilot Tx power       | 23 dBm    |
| System bandwidth        | 256 MHz   | UE antenna pattern      | Omnidirectional |
| Subcarrier number       | 128       | BS antenna pattern      | Cosine response |

the Fresnel equation and reflections with up to five bounces are taken into account. The relative permittivities of building walls are uniformly distributed between 3 and 7. There are 8 mMIMO BSs equipped with ULAs, each has 16 elements with half-wavelength spacing. The antenna arrays of the BSs are oriented perpendicular to the building surfaces where the BSs are mounted. We collect CSI samples from $U = 1425$ unknown positions among UE traces and the average distance between neighboring sampled locations is approximately 2 m. A covariance matrix is estimated over 32 realizations of the channel vector $h$ over multiple adjacent subcarriers. For semi-supervised learning, additional $L = 75$ samples are generated randomly on the roads. More simulation parameters are listed in Table 1. To measure the performance of CSI-based localization methods, we use the mean localization error (MLE) metric, which is $MLE = \frac{1}{U} \sum_{n=1}^{U} \| h_{L+n} - y_{L+n} \| _2$.

B. Algorithm Parameters

First, with a fixed perplexity $k_t$, we run the St-SNE algorithm with different learning rate $\eta$ and momentum $\alpha$. We found that a small $\eta$ will take more iterations for St-SNE to converge, while a large $\eta$ cannot find a local minimum for the cost function. It turns out that $\eta = 1000$ is a suitable option after trial and error. We use a typical momentum $\alpha = 0.6$ as in [19] to accelerate the optimization process. Fig. 3 shows that with such a setting, the algorithm converged after about 1500 iterations. So we set $T = 2000$ the max iteration number. We then change the perplexity $k_t$ and run the algorithm 10 times. The MLE vs perplexity curve is shown in Fig. 4. A small perplexity will lead to the so called Crowding problem [19].

C. Performance Comparison

We now investigate the performance of the proposed St-SNE method for mmWave localization in more detail, and compare it with kNN [20] and semi-supervised Laplacian Eigenmap (SLE) [18] method. kNN is widely used in RSSI-based and CSI-based fingerprinting. Though kNN is quite simple, recent research shows that it demonstrated the best performance in localization accuracy among a wide range of machine learning methods in a complex environment [21]. SLE is shown to be better than kNN in [18]. For kNN, a small $k$ can obtain good performance [20] and we use $k = 3$ neighbors which achieves smallest MLE in kNN here.

The localization results with these three methods are illustrated in Fig. 5 and the Cumulative Distribution Functions (CDF) of localization errors are shown in Fig. 6. Compare the maps in Fig. 5 to the ground-truth map in Fig. 2, we see that positions of points far from the labeled anchors cannot be accurately estimated via kNN and SLE. It can be seen in Fig. 6 that about 23% of unlabeled points have a localization error larger than 15 m. Compared to kNN and SLE, St-SNE greatly reduces the errors of those points, with only 7% of unlabeled points having a error larger than 15 m, leading to approximate 38% and 35% localization error reductions.

V. Conclusions

We have proposed a machine learning method St-SNE for mmWave multi-cell mobile localization. This method directly embeds the high-dimensional multi-antenna CSI samples into the 2D geographical map by governing the self-learning process of t-SNE with a few position labels. Through experiments in a simulated urban outdoor mmWave localization methods, we use the mean localization error (MLE) metric, which is

$$MLE = \frac{1}{U} \sum_{n=1}^{U} \| z_{L+n} - y_{L+n} \| _2.$$
network, we have shown that St-SNE is able to perform accurate large-scale mmWave localization for scenarios with realistic UE distributions, even with a small portion of labeled data. St-SNE is scalable and automatic in the sense that it could be implemented for multi-cell networks, with spatially sparse labeled samples, and does not require accurate network synchronization. One drawback of St-SNE is its high computation complexity compared with kNN and SLE. A prospective research direction would be to use a graph or tree method to accelerate its computation of the probability matrices.

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