ESTIMATING THE MYOCARDIUM’S ANGLE OF THREE-DIMENSIONAL TRAJECTORY, USING THE TRACKING OF SEQUENTIAL TWO-DIMENSIONAL ECHOCARDIOGRAPHY IMAGES

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BACKGROUND: In this study, the angle of the myocardium’s trajectory in three dimensions (Φ) was estimated by simultaneous use of long-axis and short-axis views of left ventricle septum two-dimensional images. Then correlation of three-dimensional trajectory’s angle with the rotation angle from the long (χ) and short (θ) axis views was estimated and compared at the three levels of base, mid and apex of the interventricular septum wall.

METHODS: Two-dimensional echocardiography images of long- and short-axis views of 19 healthy men were recorded and analyzed. Using an electrocardiogram of each individual, the images of the two views were synchronized. The interventricular septum wall motion at the three levels of base, mid and apex was estimated, using a block matching algorithm throughout three cardiac cycles. Considering the defined system of coordinates and the position vectors in long and short-axis views, the 3-dimensional angle of the trajectory was calculated.

RESULTS: Maxima of the Φ, θ, and χ angles were extracted at 16.33 ± 3.01, 10.61 ± 3.38, and 15.11 ± 3.30 degrees at base level, 22.77 ± 4.95, 7.78 ± 2.96, and 16.72 ± 2.66 degrees at mid level and 14.60 ± 5.81, 10.37 ± 5.48, and 8.79 ± 3.32 degrees at apex level, respectively, of the septum wall, respectively. This study shows significant correlation between the angle of 3-dimensional trajectory (Φ) with the angle in short axis view (θ) of the septum wall at the apex level; and also with the angle in long axis view (χ) of the septum wall at base and mid levels.

CONCLUSION: Due to the motion of the wall of the left ventricle in three dimensions, and the non-isotropic structure of myofibers, the angle of 3-dimensional trajectory was estimated using the speckle tracking method of 2-dimentional echocardiography images.

KEY WORDS: Echocardiography · Torsion angle · Three-dimensional · Image processing · Myocardium.

INTRODUCTION

General performance parameters of the left ventricle (LV), such as the ejection fraction, cannot differentiate the local changes caused by different physiological conditions. Local study of the left ventricular performance was carried out by quantification of the myocardium trajectory, using the parameters of strain, strain rate and stress. The helix structure of the myofibers of myocardium and the change of these myofibers’ angle along the wall thickness, lead to torsional motion of the ventricle (apex rotational motion in the opposite direction of the base). According to the Torrent-Gausp model, the left ventricular tissue consists of two descending (clockwise) and ascending (counter-clockwise) branches which form the base section at first, then descend spirally, and ascend to the aorta. In addition to the uniform distribution of stress and shortening along the fibers, torsion also plays a major role in the ejection fraction of the heart. So with a shortening of myofibers of about only 15–20%, the heart’s ejection fraction is estimated at 50–60%. Any torsional disorders increase the stress and strain in the inner layer, hence increasing the demand for oxy-
gen, and ultimately decreasing the systolic performance of the LV. Thus, the potential characteristic of measuring LV torsion may be an early diagnosis of myocardial damage.

The quantification of such motion has been done using the angle of rotation, torsion angle and circumferential-longitudinal shear angle with invasive implantation of tantalum markers and X-ray imaging, and non-invasive techniques such as magnetic resonance imaging (MRI) and echocardiography. The measurement of torsion in echocardiography images was initially done using the tissue Doppler technique. The latest technique for the measurement of the torsion angle is using the block matching algorithm to track sequential echocardiography images, which does not have the problems associated with the tissue Doppler technique. Despite the 3-dimensional motion of the myocardium, this angle has so far been estimated in echocardiography images by eliminating the longitudinal motion in 2-dimensional short-axis view images and by eliminating the circumferential motion in 2-dimensional longitudinal view images. Despite many studies about the left ventricular angle of rotation on a two-dimensional scale, there are as yet, no studies about the introduction and extraction of the torsion angle of myocardial levels on a 3-dimensional scale.

Thus in the current study, 2-dimensional echocardiography images are first synchronized for two short-axis and longitudinal-axis views, using the view’s electrocardiogram (ECG) signals. The sequential echocardiography images are then processed, using the block matching algorithm. Coordination of the interventricular septum trajectory will be estimated at the three levels of base, mid and apex. Since the quality of images is very important for the accuracy of tracking, the highest quality images of the base, mid and apex levels of the septal wall are used. After extracting the 3-dimensional trajectory, the angle of the left ventricular 3-dimensional trajectory will be estimated, considering 3-dimensional trajectory vectors. The correlation between the 3-dimensional angle of trajectory in the base, mid and apex levels of the interventricularseptal wall, and extracted rotation angles from both the short-axis and longitudinal axis views, will be analyzed and assessed.

**METHODS**

**SUBJECTS**

Nineteen adult males (46 ± 6 years old), who based on echocardiography examinations, had a healthy heart, volunteered to participate in this study. Based on Framingham study indices, including a person’s gender, age, blood pressure, smoking, blood cholesterol levels, having diabetes and hypertrophy, the risk of developing coronary artery disease in the volunteered participants was less than 10%. Each healthy individual underwent normal physical examinations, including blood pressure measurements, echocardiographic general parameters studies, and recording of ECG signals, at the same time as echocardiography imaging. The volunteered individuals had no history of cardiovascular diseases, angina, high blood pressure, or diabetes, and were not taking any medication. Before echocardiography imaging, the blood pressure of the individuals was measured in the supine position, using a Microfile_BP 3BU (Microfile, Heerbrugg, Switzerland) calibrated oscillometric sphygmomanometer with a blocking cuff (±1 mmHg, 30–280 mmHg). General performance parameters of the heart, including linear measurements of ventricular dimensions and the left atrium of heart, were then extracted in longitudinal parasternal and apical four-chambers views, using M-mode and B-mode ultrasound imaging techniques. The ventricular diastolic performance was also extracted, using blood flow parameters of the mitral valve, with spectral Doppler imaging technique. Before the test, informed participation consent was received from all the volunteers. This protocol was approved by the medical ethics committee of Tarbiat Modares University.

**IMAGING AND EXTRACTING THE MYOCARDIAL MUSCLE MOVEMENT STAGE**

After a general examination of the subjects, tissue harmonic imaging (transmitted frequency of 1.7 MHz and received frequency of 3.4 MHz) was done using an echocardiography system (Philips iE33 xMATRIX, Best, Netherlands) with electronic ultrasonic transducer (S5-1), and 75–95 frames per second in Digital Imaging and Communications in Medicine format, a spatial resolution of 0.26 ± 0.01 mm, and a maximum depth of study of 12 to 16 cm. Echocardiography images were recorded from the longitudinal four chambers and short-axis views at the three apex, mid and base levels according to the standards of the American Heart Association (AHA). To remove artifacts caused by movement of the diaphragm, the volunteers were asked to hold their breath during the recording of three cardiac cycles of echocardiography images. After transferring the sequential echocardiography images to the computer, with a minimum temporal resolution of 14 ms, the mid-ventricular septal wall was tracked based on the AHA sixteen segments standard model, using the block matching algorithm, in three cardiac cycles at the three base, mid and apex levels, and the average of these three measurements, with an error of less than 10%, was considered as the output. Low quality images that had artifacts, due to the movement of diaphragm or the subjects during the imaging process, were removed from the study.

In the block matching algorithm, after reading images of a cardiac cycle as the input, the region of interest (ROI) in the source images was then selected by the user. Considering the size of the ROI and its location in the source image, the search area was defined in dimensions twice as large as the area of the ROI, centered on the location of the ROI in the target image. In the next stage, the sum of absolute difference (SAD) quan-
tity between the ROI, and all blocks with the same size was calculated in the search area. The location of the block with the minimum SAD was selected as the location of the ROI in the target image.\(^{10}\)

According to the flowchart shown in Fig. 1, the ROI is selected by the user in the first frame, and the block corresponding to the minimum SAD is found in the second frame (Fig. 2). In order to select the corresponding block in the third frame, a block that has the minimum SAD, compared to the block that was found in the second frame, would be selected and so forth.

After the execution of the block matching algorithm, considering the geometric model of the heart as an truncated ellipsoid (Fig. 3A),\(^{2}\) and the geometry of the taken views, the coordinates \((X_{\text{image}}, Y_{\text{image}}}) (Fig. 3B) and \((Z_{\text{image}}, Z_{\text{image}}}) (Fig. 3C) were achieved, relative to the image coordinate system.

The reference coordinate system was considered as shown in Fig. 3 by selecting the center of the mid-level of the LV as the origin of the coordinates and choosing the orientation of its axes. The center of ventricle \((X_0, Y_0) (Fig. 3B)\) was identified in short-axis view on coordinates of the image using Fiji software (http://fiji.sc) (the image processing software package for bioscience researchers), by fit of circular or oval shapes on segments of the LV anatomical images. The origin of coordinates \((Z_0, Z_0) (Fig. 3C)\) was identified in longitudinal axis view, using the anatomical papillary muscle marker. At the end of this stage, the coordinates of the myocardium’s septum were transferred, from the coordinates system defined in the image, to the reference coordinate system (equations 1–4).

\[
\begin{align*}
1) X_{\text{new}} &= X_{\text{image}} - X_0 \\
2) Y_{\text{new}} &= Y_{\text{image}} - Y_0 \\
3) Z_{\text{new}} &= Z_{\text{image}} - Z_0 \\
4) \Delta Z_{\text{new}} &= \Delta Z_{\text{image}} - \Delta Z_0
\end{align*}
\]

Fig. 1. Process view of the block matching program. ROI: region of interest, SAD: sum of absolute difference.

Fig. 2. Implementation of block matching algorithm. Region of interest (ROI) is selected by the user in the first image and the second image corresponding block is the minimum sum of absolute difference. Sample ROI search (frame 78) (A) and destination (frame 112) (B) in the septal segment echocardiographic images based on the 4-chamber view is specified.
**Synchronization of the LV views in both longitudinal and lateral axes**

Longitudinal and short-axis views were imaged with a 2–3 min delay from the heart of each individual. Due to the changes of heart rate during successive cycles of the heart and unequal frame rates in both views in this study, combining the images in short-axis view with the ones taken in longitudinal axis view needed examination of the synchronization of the short- and long-axis views data using the ECG signal. Therefore, the ECG signal was extracted from the echocardiography images using this signal in such images and color images processing. In order to extract this signal, the changes of heart rate during successive cycles of the heart and long-axis views data using the ECG signal. The average of angle changes for three cardiac cycles was obtained from equation 5:

\[
\chi(t) = \sin^{-1}\left(\frac{\vec{a} \times \vec{b}}{|\vec{a}| \cdot |\vec{b}|}\right) = \sin^{-1}\left[ \frac{\sqrt{(a_x \cdot b_x - a_y \cdot b_y)^2}}{\sqrt{(a_x^2 + a_y^2) \cdot \sqrt{(b_x^2 + b_y^2)}}} \right]
\]

\[
\vec{a} = (a_x, a_y) \quad \text{and} \quad \vec{b} = (b_x, b_y)
\]

To obtain the coordinates of the last pixel of the ECG signal, the transformation was performed by transferring these values to the Excel software. Signals recorded in long and short-axis views were compared visually after the extraction of the ECG signal in both these views of echocardiography images. The differences were observed in the end of the diasstolic phase for most of the images. In images where such differences were high, the repeated frames in different phases of the cardiac cycle were removed due to inequality in the size of such differences for different phases of ECG signal in order to synchronize the data. The output data in this stage were used to calculate the short-axis, long-axis angles and angle of 3-dimensional trajectory.

**Calculating angles**

Considering the defined system of coordinates, \(\vec{a} = (a_x, a_y)\) and \(\vec{b} = (b_x, b_y)\) are position vectors in long-axis view. Thus, the rotation angle in long-axis view \(\theta(t)\) is obtained from equation 6:

\[
\theta(t) = \sin^{-1}\left(\frac{\vec{a} \times \vec{b}}{|\vec{a}| \cdot |\vec{b}|}\right) = \sin^{-1}\left[ \frac{\sqrt{(a_x \cdot b_x - a_y \cdot b_y)^2}}{\sqrt{(a_x^2 + a_y^2) \cdot \sqrt{(b_x^2 + b_y^2)}}} \right]
\]

\[
\vec{a} = (a_x, a_y, a_z) \quad \text{and} \quad \vec{b} = (b_x, b_y, b_z)
\]

The average of angle changes for three cardiac cycles was then extracted as the output of this stage. In order to perform statistical comparison of the results, the maximum angle of 3-dimensional trajectory \(\Theta(t)\), and maximum angles of rotation in short-axis \(\theta(t)\) and long-axis \(\lambda(t)\) were reported as the average ± standard deviation. Pearson’s analysis of correlation with a significance level of less than 0.05 was used to study the correlation between \(\theta(t), \lambda(t)\) and \(\Theta(t)\). The sample size was estimated with a confidence level of 95% and power of test of 90% in each group. The statistical analysis was done using SPSS 16 software (SPSS Inc., Chicago, IL, USA).

**RESULTS**

The demographic and echocardiographic measures of 19 men with an average age of 46 ± 5 years are given Table 1. The general parameters extracted from Table 1 shows the healthiness of heart in individuals of this study.

Recorded ECG signals in the short and long axis views im-
ages were visually compared for each individual, during three cardiac cycles. Due to the non-synchronization of three cardiac cycles in two recorded views, repeated data in different phases of the cardiac cycle were removed. Fig. 4A was drawn before synchronization, and Fig. 4B was drawn after synchronization of the images, in both short and longitudinal axes views.

Fig. 5 shows the changes in location of the septum segment in base (Fig. 5A), mid (Fig. 5B), and apex (Fig. 5C), separately, for a sample individual, obtained by averaging the data of three cardiac cycles. The location of the septal wall is presented in three base, mid and apex levels, using x, y, and z coordinates relative to the origin, for the mid-level of the LV in pixels.

The changes of x, y coordinates in three base, mid and apex levels of the septal wall are consistent with ventricular contraction and relaxation. The changes in x are associated with big standard deviations due to small movements and tracking error.

| Parameters                                      | Mean ± SD     |
|-------------------------------------------------|---------------|
| Body mass index (kg/m²)                         | 26.2 ± 2.0    |
| Heart rate (bpm)                                | 75 ± 5        |
| Diastolic pressure (mmHg)                       | 72 ± 14       |
| Systolic pressure (mmHg)                        | 111 ± 13      |
| Diastolic LV posterior wall (mm)                 | 11.9 ± 1.5    |
| Systolic LV posterior wall (mm)                  | 16.4 ± 2.9    |
| Interventricularseptal diastolic dimension (mm) | 12.0 ± 1.8    |
| Interventricularseptal systolic dimension (mm)   | 15.7 ± 3.0    |
| Fractional shortening (%)                       | 41.12 ± 9.54  |
| Ejection fraction (%)                            | 62.92 ± 9.82  |
| Diastolic LV large diameter (mm)                 | 79.5 ± 5.5    |
| Systolic LV large diameter (mm)                  | 64.0 ± 5.0    |

The averages and standard deviations of \( \chi_M, \theta_M, \) and \( \Phi_M \) during three cardiac cycles for the interventricular septal wall in healthy individuals in this study are presented in Fig. 7, for the three base, mid and apex levels in degrees.

Considering Fig. 7, the bigger magnitude of \( \Phi_M \) in all three base, mid and apex levels compared to the other two angles is clearly obvious. \( \theta_M \) is smaller than the other two angles in both base and mid-levels which suggests a large septal wall movement in the longitudinal direction, compared to the short-axis direction. \( \theta_M \) was obtained bigger than the \( \chi_M \) angle in the apex level, and considering its large standard deviation, it requires further investigation.

After studying the normality of data (Shapiro-Wilk test), the correlations between \( \chi_M \) and \( \Phi_M \), and also angle \( \theta_M \) in the three base, mid and apex levels were analyzed, using Pearson’s analysis of correlation (Fig. 8). A highly significant correlation was observed between the two \( \theta_M \) and \( \Phi_M \) in the apex level (\( r = 0.82, p = 0.03 \)). The results showed a significant correlation between \( \chi_M \) and \( \Phi_M \) in the base level of the interventricular-

Changes of z coordinates in both base and mid-levels are consistent with systolic and diastolic ventricular phases but are opposite to the expected positive direction of z in the apex level. Changes of z coordinates in the three base, mid and apex levels suggest that the septal wall contracts during the cardiac cycle, while moving in the direction of negative z (the direction of the apex). The average rates of temporal changes of \( \chi, \theta \) and \( \Phi \) during three cardiac cycles for the mid-ventricular septal wall of a healthy individual are presented in Fig. 5 for three base (Fig. 6A), mid (Fig. 6B), and apex (Fig. 6C) levels in degrees.

Considering the positivity contract of counter-clockwise direction forms the apex point of view for \( \theta \), and negativity contract form perpendicular to the plane \((LZ, Z)\) point of view for \( \chi \), the counter-clockwise rotation of the apex and clockwise rotation of the base are in agreement with the results of previous studies. Due to the non-definition of a unique direction for \( \Phi \), its magnitude is shown.
Fig. 5. Temporal changes of the location of septal wall coordinates in three directions of x (left), y (middle), and z (right) in three base (A), mid (B) and apex (C) levels in pixels, during the cardiac cycle (the horizontal axis represents the frame number of the image).

Fig. 6. The pattern of the moment changes for $\chi$ (right), $\theta$ (middle) and $\Phi$ (left) during a cardiac cycle in three base (A), mid (B), and apex (C) levels of the interventricular septal wall.
septal wall \( (r = 0.57, p = 0.03) \) and in the mid-level of the interventricular septal wall \( (r = 0.79, p = 0.01) \).

The regression function between \( \theta_{\text{M}} \) and \( \Phi_{\text{M}} \) angles in the apex level was estimated as \( \Phi_{\text{M}} = 0.87 \times \theta_{\text{M}} + 5.57 \). The regression function between \( \chi_{\text{M}} \) and \( \Phi_{\text{M}} \) angles was estimated as \( \Phi_{\text{M}} = 0.35 \times \chi_{\text{M}} + 11.09 \) in the base level of the interventricular septal wall and as \( \Phi_{\text{M}} = 1.46 \times \chi_{\text{M}} - 1.62 \) in the mid-level of the interventricular septal wall. There was no significant correlation between \( \theta_{\text{M}} \) and \( \Phi_{\text{M}} \) angles, in both base and mid-levels. \( \Phi_{\text{M}} \) and \( \chi_{\text{M}} \) angles had no significant correlation in apex level.

**DISCUSSION**

Quantification of the LV motion were primarily based on simplified geometrics such as cylinder and truncated ellipsoid by considering the isotropic myofiber structure. The geometric model of ellipsoid with isotropic myofiber structure was used in the current study, which is the closest simple geometric model to the actual ventricular geometry. The LV’s motion has been estimated by applying differential and area matching algorithms on sequential 2-dimensional echocardiography or MRI images. The rotation angles for different segments were estimated using short-axis view images in two dimensions, and the mean of angles was considered as the rotation angle, for each level. The torsion angle (difference of angles in two base and apex levels), is a general parameter and depends on the changes in the whole ventricle. Since ventricle motion takes place in circumferential, radial and longitudinal directions, and because of the possibility of change in pattern of the ventricle motion in only a particular direction, the rotation and torsion angles may not be sensitive enough in different physiological conditions. In order to have a parameter that includes all three directions, and reflects their changes, \( \Phi \) was defined and estimated. A block matching algorithm was used.

Factors such as changes in the shape of tissue, image noise, speckle non-correlation, off-the-screen motion, and artifacts caused by speckle motion, have restricted the use of block matching in ultrasonic images.

Results of correlation between \( \Phi_{\text{M}} \) with \( \theta_{\text{M}} \) and \( \chi_{\text{M}} \) showed a significant correlation between the \( \Phi_{\text{M}} \) and \( \theta_{\text{M}} \) of apex level. Also \( \Phi_{\text{M}} \) and \( \chi_{\text{M}} \) were significantly correlated in both base and mid-levels. The non-correlation between the \( \Phi_{\text{M}} \) and \( \theta_{\text{M}} \) in both base and mid levels, and also the non-correlation between \( \Phi_{\text{M}} \) and \( \chi_{\text{M}} \) in apex level could be due to specific orientation of fibers in those regions. According to Torrent-Gausp model, the fibers in base and mid regions of septum have longitudinal orientation and the fibers in its apex segment have circumferential orientation. Therefore, motion in base and mid levels of septal wall will be affected by longitudinal fibers and the \( \chi \) has a bigger contribution in \( \Phi \). The motion of septal wall is also affected by circumferential fibers in apex level; therefore \( \theta \) has a bigger contribution in \( \Phi \).

Gustafsson et al. reported the magnitude of \( \theta \) as \(-8.8 \pm 3.5^\circ \) in the base, \(-2.3 \pm 3.0^\circ \) in the mid, and \(11.1 \pm 4.4^\circ \) in the apex levels. \( \theta_{\text{M}} \) of the interventricular septum in the current study was estimated as \(-10.61 \pm 3.38^\circ \) in the base, \(-7.78 \pm 2.96^\circ \) in the mid, and \(10.37 \pm 5.48^\circ \) in the apex segments. The range and sign of angles in both base and apex levels are in agreement with Gustafsson et al. A great difference is ob-

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**Fig. 7.** \( \chi_{\text{M}}, \theta_{\text{M}}, \) and \( \Phi_{\text{M}} \) during three cardiac cycles for the interventricular septal wall in healthy individuals for three base, mid and apex levels, in degrees.

**Fig. 8.** Study of the correlation between \( \chi_{\text{M}} \) and \( \Phi_{\text{M}} \) in base (A) and mid-levels (B) and \( \theta_{\text{M}} \) and \( \Phi_{\text{M}} \) in the apex level (C).
served in mid-level that is probably associated with the lack of an accurate definition of mid-level. During the only study that was conducted in long-axis view, Arab-Baferani et al.\(^\text{16}\) estimated \(\chi_M\) as 18.51 ± 3.41° in the base, and 14.74 ± 2.91° in the apex levels. \(\chi_M\) of the interventricular septum was estimated as 15.11 ± 3.30° in the base, 16.72 ± 2.66° in the mid, and 8.79 ± 5.82° in the apex segments, respectively. It seems that the difference for apex level is associated with the lack of an accurate definition of this level, and tracking error, due to low quality of images. It should be noted that no standard value has yet been defined for \(\chi_M\) and \(\theta_M\).

The magnitude of \(\Phi_M\) was estimated as 16.33 ± 3.01° in the base, 22.77 ± 4.95° in the mid, and 14.60 ± 5.81° in the apex levels. Urbano Moral et al.\(^\text{20}\) reported the average rotation in the base and apex levels as -2.6 ± 1.6° and +8.2 ± 3.6°, respectively using the speckle tracking of 3-dimensional echocardiography images. This study was carried out using an Artida 4D system (Toshiba Medical Systems, Tustin, CA, USA) that according to the instructions of its manufacturer, measures the rotation in two base and apex levels. Thus, the obtained results cannot be compared with the results of this study.

Due to the low temporal resolution of 3-dimensional images during echocardiography in the current study, and the impossibility of saving raw 3-dimensional images, the combination of 2-dimensional images was used. While having the advantage of high temporal resolution, this approach does however increase the error for finding the location of the desired segment in images of longitudinal view, and their corresponding segment in short-axis view, and suffers from imaging in two different times. Thus, using real-time 3-dimensional images can be an effective way to remove some of these factors. It is suggested that such angle is measured using real-time 3-dimensional images and the capability of \(\Phi\) to identify the physiological conditions of healthy and unhealthy hearts compared to the other two angles, will be examined.

In conclusion, due to the motion of the wall of the LV in three dimensions, and the non-isotropic structure of myocardium, it is possible that in different physiological conditions, any measurable change only happens during the motion of myocardial muscle in one of the longitudinal, circumferential or radial directions. Therefore, a parameter dependent on the motion in three directions can be helpful. So, \(\Phi\) for myocardial muscle was defined using the speckle tracking method of 2-dimensional echocardiography images in both short-axis and long-axis views and estimated in three base, mid and apex levels of the septal wall. The significant correlation between this angle and \(\theta\) and \(\Phi\) show that this angle can be used to study the behavior of the myocardial muscle in different pathological conditions.

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### References

1. Geyer H, Caracciolo G, Abe H, Vilansky S, Carerj S, Gentile F, Nesser HJ, Khandheria B, Narula J, Sengupta PP. Assessment of myocardial mechanics using speckle tracking echocardiography: fundamentals and clinical applications. J Am Soc Echocardiogr 2010;23:351-69; quiz 453-5.
2. Taber LA, Yang M, Podsuzan WW. Mechanics of ventricular torsion. J Biomech 1996;29:745-52.
3. Sengupta PP, Krishnamoorthy VK, Koziniec J, Narula J, Vannan MA, Lester SJ, Tajik AJ, Seward JB, Khandheria BK, Belohlavek M. Left ventricular form and function revisited: applied translational science to cardiovascular ultrasound imaging. J Am Soc Echocardiogr 2007;20:539-51.
4. Torrent-Guasp F, Ballester M, Buckberg GD, Carreras F, Flotats A, Carrió I, Ferreira A, Samuels LE, Narula J. Spatial orientation of the ventricular muscle bundle: physiologic contribution and surgical implications. J Thorac Cardiovasc Surg 2001;122:389-92.
5. Nakatani S. Left ventricular rotation and twist: why should we learn? J Cardiovasc Ultrasound 2011;19:1-6.
6. Buckberg GD. Basic science review: the helix and the heart. J Thorac Cardiovasc Surg 2002;124:863-83.
7. Sengupta PP, Tajik AJ, Chandraselkaran K, Khandheria BK. Twist mechanics of the left ventricle: principles and application. JACC Cardiovasc Imaging 2008;1:366-76.
8. Esch BT, Wärburton DE. Left ventricular torsion and recoil: implications for exercise performance and cardiovascular disease. J Appl Physiol (1955) 2009;106:362-9.
9. Hansen DE, Daughters GT 2nd, Alderman EL, Stinson EB, Baldwin JC, Miller DC. Effect of acute heart failure allograft rejection on left ventricular systolic and diastolic recoil measured by intramyocardial markers. Circulation 1987;76:998-1008.
10. Ingels NB Jr, Daughters GT 2nd, Stinson EB, Alderman EL. Measurement of midwall myocardial dynamics in intact man by radiography of surgically implanted markers. Circulation 1975;52:859-67.
11. Gustafsson U, Lindqvist P, Mörner S, Waldenström A. Assessment of regional rotation patterns improves the understanding of the systolic and diastolic left ventricular function: an echocardiographic speckle-tracking study in healthy individuals. Eur J Echocardiogr 2009;10:56-61.
12. Rüssel IK, Götte MJ, Kuijer JP, Marcus JT. Regional assessment of left ventricular torsion by CMR tagging. J Cardiovasc Magn Reson 2008;10:26.
13. Garot J, Pascal O, Déhöld B, Derumeaux G, Gerber BL, Dubois-Randé JL, Lima JA, Guéret P. Alterations of systolic left ventricular twist after acute myocardial infarction. Am J Physiol Heart Circ Physiol 2002;282:H357-62.
14. Helle-Valle T, Remme EW, Lyseggen E, Pettersen E, Vartdal T, Opdahl A, Smith HJ, Osman NF, Iltien H, Edvardsen T, Smiseth OA. Clinical assessment of left ventricular rotation and strain: a novel approach for quantification of function in injured myocardium and its border zones. Am J Physiol Heart Circ Physiol 2009;297:H2357-67.
15. Notomi Y, Lysyansky P, Setser RM, Shiono T, Popovic ZB, Martin-Miklovic MG, Weaver JA, Oryszak SJ, Greenberg NL, White RD, Opdahl A, Smith HJ, Osman NF, Iltien H, Edvardsen T, Smiseth OA. Clinical assessment of left ventricular rotation and strain: a novel approach for quantification of function in injured myocardium and its border zones. Am J Physiol Heart Circ Physiol 2009;297:H2357-67.
16. Arab-Baferani Z, Mohktari-Dizaji M, Roslandani E. Extraction of left ventricular torsion by two-dimensional ultrasound speckle tracking imaging. J Am Coll Cardiol 2003;43:2034-41.
17. Arab-Baferani Z, Mohktari-Dizaji M, Roslandani E. Extraction of left ventricular torsion from the long-axis view by block-matching algorithm: comparison with the short-axis view. Ultrasound 2013;21:53-52.60.
18. Wilson PW, D'Agostino RB, Levy D, Belanger AM, Silbershatz H, Kannel WB. Prediction of coronary heart disease using risk factor categories. Circulation 1998;97:1837-47.
19. Cerqueira MD, Weissman NJ, Dilisizian V, Jacobs AK, Kaul S, Laskey WK, Pennell DJ, Rumberger JA, Ryan T, Verani MS. American Heart Association Writing Group on Myocardial Segmentation
18. Guccione JM, Moonly SM, Moustakidis P, Costa KD, Moulton MJ, Ratcliffe MB, Pasque MK. Mechanism underlying mechanical dysfunction in the border zone of left ventricular aneurysm: a finite element model study. Ann Thorac Surg 2001;71:654-62.

19. Boukerroui D, Noble JA, Brady M. Velocity estimation in ultrasound images: a block matching approach. Inf Process Med Imaging 2003;18: 586-98.

20. Chen EJ, Jenkins WK, O’Brien WD Jr. The impact of various imaging parameters on ultrasonic displacement and velocity estimates. IEEE Trans Ultrason Ferroelectr Freq Control 1994;41:293-301.

21. Chadwick RS. Mechanics of the left ventricle. Biophys J 1982;39:279-88.

22. Arts T, Veenstra PC, Reneman RS. Epicardial deformation and left ventricular wall mechanisms during ejection in the dog. Am J Physiol 1982;243:H379-90.

23. Guccione JM, Moonly SM, Moustakidis P, Costa KD, Moulton MJ, Ratcliffe MB, Pasque MK. Mechanism underlying mechanical dysfunction in the border zone of left ventricular aneurysm: a finite element model study. Ann Thorac Surg 2001;71:654-62.

24. Guccione JM, Moonly SM, Wallace AW, Ratcliffe MB. Residual stress produced by ventricular volume reduction surgery has little effect on ventricular function and mechanics: a finite element model study. J Thorac Cardiovasc Surg 2001;122:592-9.

25. Yeung F, Levinson SE, Fu D, Parker KJ. Feature-adaptive motion tracking of ultrasound image sequences using a deformable mesh. IEEE Trans Med Imaging 1998;17:945-56.

26. Urbano Moral JA, Arias Godinez JA, Maron MS, Malik R, Eagan JE, Patel AR, Pandian NG. Left ventricular twist mechanics in hypertrophic cardiomyopathy assessed by three-dimensional speckle tracking echocardiography. Am J Cardiol 2011;108:1788-95.