Phat ELVIS: The inevitable effect of the Milky Way’s disc on its dark matter subhaloes

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ABSTRACT

We introduce an extension of the ELVIS project to account for the effects of the Milky Way galaxy on its subhalo population. Our simulation suite, Phat ELVIS, consists of 12 high-resolution cosmological dark matter-only (DMO) zoom simulations of Milky Way-size \( \Lambda \)CDM haloes \([M_\text{h} = (0.7–2) \times 10^{12} \, \text{M}_\odot]\) along with 12 re-runs with embedded galaxy potentials grown to match the observed Milky Way disc and bulge today. The central galaxy potential destroys subhalos on orbits with small pericentres in every halo, regardless of the ratio of galaxy mass to halo mass. This has several important implications. (1) Most of the DMO runs have no subhaloes larger than \( V_{\text{max}} = 4.5 \, \text{km s}^{-1} \) within 20 kpc and a significant lack of substructure going back \( \sim 8 \) Gyr, suggesting that local stream-heating signals from dark substructure will be rare. (2) The pericentre distributions of Milky Way satellites derived from \textit{Gaia} data are remarkably similar to the pericentre distributions of subhaloes in the DMO runs, while the DMO runs drastically overpredict galaxies with pericentres smaller than 20 kpc. (3) The enhanced destruction produces a tension opposite to that of the classic ‘missing satellites’ problem: in order to account for ultra-faint galaxies known within 30 kpc of the Galaxy, we must populate haloes with \( V_{\text{peak}} \approx 7 \, \text{km s}^{-1} (M \sim 3 \times 10^7 \, \text{M}_\odot \text{ at infall}) \), well below the atomic cooling limit of \( V_{\text{peak}} \approx 16 \, \text{km s}^{-1} (M \sim 5 \times 10^8 \, \text{M}_\odot \text{ at infall}) \). (4) If such tiny haloes do host ultra-faint dwarfs, this implies the existence of \( \sim 1000 \) satellite galaxies within 300 kpc of the Milky Way.

Key words: Galaxy: formation – galaxies: haloes – dark matter – cosmology: theory.

1 INTRODUCTION

A key prediction of standard \( \Lambda \)CDM (lambda cold dark matter) cosmology is that dark matter (DM) haloes form hierarchically. This leads to the prediction that massive DM haloes receive a continuous influx of smaller haloes as they grow. Satellite galaxies have been detected around many galaxies and clusters, including the Milky Way (MW), and these are usually associated with the most massive subhaloes predicted to exist. As \( \Lambda \)CDM cosmological simulations have progressed to higher resolution, it has become clear that the mass spectrum of substructure rises steadily towards the lowest masses resolved (e.g. Springel et al. 2008; Kuhlen, Madau & Silk 2009; Stadel et al. 2009; Garrison-Kimmel et al. 2014; Griffen et al. 2016). Testing this fundamental prediction stands as a key goal in modern cosmology. This paper aims to refine existing predictions by including the inevitable dynamical effect associated with the existence of galaxies at the centres of galaxy-size dark matter haloes.

The ‘missing satellites’ problem (Klypin et al. 1999; Moore et al. 1999) points out a clear mismatch between the relatively small number of observed MW satellites and the thousands of predicted subhaloes above the resolution limit of numerical simulations. This discrepancy can be understood without changing the cosmology by assuming that reionization suppresses star formation in the early Universe (Bullock, Kravtsov & Weinberg 2000; Somerville 2002). Such a solution matches satellite abundances once one accounts for observational incompleteness (Tollerud et al. 2008; Hargis, Willman & Peter 2014). As usually applied, these solutions suggest that haloes smaller than \( \sim 5 \times 10^8 \, \text{M}_\odot (V_{\text{max}} < 15 \, \text{km s}^{-1}) \), where \( V_{\text{max}} \) is defined as the maximum circular velocity should be dark (Thoul & Weinberg 1996; Okamoto, Gao & Theuns 2008; Ocvirk et al. 2016; Fitts et al. 2017; Graus et al. 2018a).
Detecting tiny, dark subhaloes would provide confirmation of a key prediction of ΛCDM theory and rule out many of the alternative DM and inflationary models that predict a cut-off in the power spectrum at low masses (Kamionkowski & Lidelle 2000; Bode, Ostriker & Turok 2001; Zentner & Bullock 2003; Bose et al. 2016; Bozek et al. 2016; Horiuchi et al. 2016). Since these haloes are believed to be devoid of baryons, they must be discovered indirectly. Within the Milky Way, one promising method for detecting dark subhaloes is via their dynamical effect on thin stellar streams, such as Palomar-5 and GD-1, which exist within ~20 kpc of the Galactic centre (e.g. Johnston, Spergel & Haydn 2002; Koposov, Rix & Hogg 2010; Carolberg, Griliamond & Hetherington 2012; Ngan et al. 2015; Bovy, Erkal & Sanders 2017; Bonaca et al. 2018, and references therein). With future surveys like LSST on the horizon, the number of detected streams around the MW should increase and hold information on the nature of dark substructure.

A statistical sample of MW-like haloes simulated in ΛCDM with sufficient resolution is necessary to make predictions for these observations. While several such simulations exist in the literature (e.g. Springel et al. 2008; Kuhlen et al. 2009; Stadel et al. 2009; Mao, Williamson & Wechsler 2015; Grinen et al. 2016), the vast majority are dark matter only (DMO). The use of DMO simulations to make predictions about subhalo properties is problematic because DMO simulations do not include the destructive effects of the central galaxy (D’Onghia et al. 2010). Hydrodynamic simulations show significant differences in subhalo populations compared to those observed in DMO simulations (Sawala et al. 2013, 2015; Brooks & Zolotov 2014; Wetzel et al. 2016; Zhu et al. 2016). This is particularly true in the central regions of galaxy haloes, where subhaloes are depleted significantly in hydrodynamic simulations compared to DMO counterparts (Despali & Vegetti 2017; Garrison-Kimmel et al. 2017b; Graus et al. 2018b).

Garrison-Kimmel et al. (2017b) used the high-resolution hydrodynamic ‘Latte’ simulations (Wetzel et al. 2016) to show explicitly that it is the destructive effects of the central galaxy potential, not feedback, that drives most of the differences in subhalo counts between DMO and full-physics simulations. Their analysis relied on three cosmological simulations of the same halo: (1) a full FIRE-2 physics simulations, (2) a DMO simulation, and (3) a DMO simulation with an embedded galactic potential grown to match the central galaxy formed in the hydrodynamic simulation. They showed that most of the subhalo properties seen in the full physics simulation were reproduced in the DMO plus potential runs at a fraction of the CPU cost.

In this work, we expand upon the methods of Garrison-Kimmel et al. (2017b, GK17 hereafter) to make predictions for the dark substructure populations of the Milky Way down to the smallest mass scales of relevance for current dark substructure searches ($V_{\text{max}} \simeq 4.5\, \text{km}\, \text{s}^{-1}$). Unlike the systems examined in GK17, our central galaxies are designed to match the real Milky Way disk and bulge potential precisely at $z = 0$ and are grown with time to conform to observational constraints on galaxy evolution. Using 12 zoom simulations of Milky Way size haloes, we show that the existence of the central galaxy reduces subhalo counts to near zero within ~20 kpc of the halo centre, regardless of the host halo mass or formation history. This suppression tends to affect subhaloes with early infall times and small pericentres the most. The changes are non-trivial and will have important implications for many areas that have previously been explored with DMO simulations. Some of these include the implied stellar-mass versus halo-mass relation for small galaxies (Graus et al. 2018a; Jethwa, Erkal & Belokurov 2018), quenching time-scales (Rodriguez Wimberly et al. 2018), ultra-faint galaxy completeness correction estimates (Kim, Peter & Hargis 2017), cold stellar stream heating rates (Ngan et al. 2015), predicted satellite galaxy orbits (Riley et al. 2018), and stellar halo formation (Bullock & Johnston 2005; Cooper et al. 2010). In order to facilitate science of this kind, we will make our data public upon publication of this paper as part of the ELVIS (Garrison-Kimmel et al. 2014) project site.1

In Section 2, we discuss the simulations and summarize our method of inserting an embedded potential into the centre of the host; Section 3 explores subhalo population statistics with and without a forming galaxy and presents trends with radius in subhalo depletion. We discuss further implications of our results in Section 4 and conclude in Section 5.

2 SIMULATIONS

All of our simulations are cosmological and employ the ‘zoom-in’ technique (Katz & White 1993; O’Connor et al. 2014) to achieve high force and mass resolution. We adopt the cosmology of Planck Collaboration XIII (2016): $\Omega_m = 0.6879$, $\Omega_r = 0.3121$, $h = 0.6751$. Each simulation was performed within a global cosmological box of length $50\, h^{-1}\, \text{Mpc} = 74.06\, \text{Mpc}$. We chose each high-resolution region to contain a single MW-mass ($\sim 10^{12}\, \text{M}_\odot$) halo at $z = 0$ that has no neighbouring haloes of similar or greater mass within 3 Mpc. We focus on 12 such haloes, spanning the range of halo mass estimates of the MW summarized in Bland-Hawthorn & Gerhard (2016): $M_h = (0.7-2)\times 10^{12}\, \text{M}_\odot$. Haloes were selected based only on their viral mass with no preference on merger history or to the subhalo population. The high-resolution regions have dark matter particle mass of $m_{\text{DM}} = 3 \times 10^4\, \text{M}_\odot$ and a Plummer equivalent force softening length of 37 pc. This allows us to model and identify subhaloes conservatively down to maximum circular velocity $V_{\text{max}} > 4.5\, \text{km}\, \text{s}^{-1}$, which corresponds to a total bound mass $M \gtrsim 5 \times 10^6\, \text{M}_\odot$.

We ran all simulations, using gizmo (Hopkins 2015), which uses an updated version of the TREE+PM gravity solver included in gadget-3 (Springel 2005). We generated initial conditions for the simulations at $z = 125$ using music (Hahn & Abel 2011) with second-order Lagrangian perturbation theory. We identify halo centres and create halo catalogues with rockstar (Behroozi, Wechsler & Wu 2013a) and build merger trees using consistent-trees (Behroozi et al. 2013b) based on 152 snapshots spaced evenly in a scale factor. The merger trees and catalogues allow us to identify basic halo properties at each snapshot, including the maximum circular velocity $V_{\text{max}}$ and viral mass $M_v$ for the main progenitor of each host halo and subhalo. For each subhalo, we record the time it first fell into the viral radius of its host and also the largest value of $V_{\text{max}}$ it ever had over its history, $V_{\text{peak}}$. In most cases $V_{\text{peak}}$ occurs just prior to first infall.

For the embedded disc galaxy simulations, we insert the galaxy potentials at $z = 3$ (lookback $\sim 11.7\, \text{Gyr}$), when galaxy masses are small compared to the main progenitor (typically, $M_{\text{gal}}/M_v(z = 3) \simeq 0.03$). Prior to $z = 3$, the DISC and DMO simulations are identical. At $z = 3$, we impose the galaxy potential, which is centred on a sink particle with softening length 0.5 kpc and mass $10^8\, \text{M}_\odot$. The sink particle is initially placed in the centre of the host halo, as determined by rockstar. We have found that dynamical friction keeps the sink particle (and thus the galaxy potential) centred on the

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1http://localgroup.ps.uci.edu/phat-elvis/
2http://www.tapir.caltech.edu/~phopkins/Site/GIZMO.html
Table 1. Parameters for the Milky Way potential components at $z = 0$ used in every DMO run. The disc scale radii correspond to exponential disc radii, which we model analytically by summing three Miyamoto & Nagai (1975) disc potentials following Smith et al. (2015). The bulge radius corresponds to the scale radius of a Hernquist (1990) potential. Parameters were taken from McMillan (2017) and Bland-Hawthorn & Gerhard (2016).

| Component   | Mass ($10^{10} M_\odot$) | Scale radius (kpc) | Scale height (kpc) |
|-------------|--------------------------|--------------------|--------------------|
| Stellar disc| 4.1                      | 2.5                | 0.35               |
| Gas disc    | 1.9                      | 7.0                | 0.08               |
| Bulge       | 0.9                      | 0.5                | —                  |

host halo throughout simulations – with a maximum deviation from centre of $\sim 150$ pc at $z = 0$. Host halo mass accretion rates, positions, and global evolution are almost indistinguishable from the DMO runs after the galaxy potentials are included. As discussed below, the galaxy potential grows with time in a way that tracks dark matter halo growth. All galaxy potentials at $z = 0$ are the same, with properties that match the Milky Way today, as summarized in Table 1. This means that our higher $M_\text{h}$ halos will have smaller $M_\text{gal}/M_\text{h}$ ratios, where $M_\text{gal} = M_\text{stellar disc} + M_\text{gas disc} + M_\text{bulge}$. The full range of our suite is $M_\text{gal}/M_\text{h} \approx 0.35 \pm 0.1$.

The properties of our 12 pairs of host haloes, along with the number of resolved subhaloes identified by rockstar within several radial cuts of that host, are listed in Table 2. The first column lists the name of each simulated halo. The names are inspired by the 12 greatest songs recorded by the Elvis Presley over his 24-yr musical career. Haloes are listed in DMO/disc-run pairs, such that the disc simulations are identified with an added ‘Disc’ to the name. Virial masses and radii (columns 2 and 3) use the Bryan & Norman (1998) definition of virial mass. Columns 4 and 5 list $V_{\text{max}}$ and virial velocity, $V_c$. Columns 6–9 give the cumulative count of subhaloes with $V_{\text{max}} > 4.5$ km s$^{-1}$ within 25, 50, 100, and 300 kpc of each host’s centre. As we discuss below, the difference in subhalo counts between the Disc runs and DMO runs is systematic and significant, especially at small radii. Column 10 lists the best-fitting Navarro, Frenk & White (1997, NFW) concentration for each halo. Note that the Disc runs are always more concentrated, even though their formation times (column 11) are similar. This is particularly true of the lower mass host halos. The reason is that the dark matter is the host haloes contract in response to the central galaxy.

Throughout this work, we characterize subhaloes in terms of their $V_{\text{max}}$ and $V_{\text{peak}}$ (peak $V_{\text{max}}$). We do this because we have found $V_{\text{max}}$ selection to produce more consistent results between halo finders (e.g. rockstar and AHF) than mass selection (for subhaloes in particular, mass definitions are more subjective). For reference, Garrison-Kimmel et al. (2014) found median relations between velocity and mass of $M_{\text{peak}}/M_\odot \approx 9.8 \times 10^2 (V_{\text{peak}}/10$ km s$^{-1})^{3.33}$ and $M/\odot \approx 9.1 \times 10^2 (V_{\text{max}}/10$ km s$^{-1})^{3.45}$.

### 2.1 Embedded potentials

The effects of the central baryonic disc is included in the DMO simulations following the basic technique described in Garrison-Kimmel et al. (2017b). Our embedded potentials are more detailed than those used by GK17 in order to more accurately model the MW galaxy. Specifically, we include an exponential stellar disc, an exponential gaseous disc, and a Hernquist bulge component. The galaxy potentials evolve from high redshift using empirically motivated scaling relations (see 2.1.1) and we force them to match currently observed MW properties at $z = 0$. These $z = 0$ properties are taken from McMillan (2017) and Bland-Hawthorn & Gerhard (2016) as summarized in Table 1. For simplicity, we hold all disc orientations fixed throughout the simulation. The analysis in Section 3.4 of GK17 suggests that the results do not largely depend on the orientation or shape of the embedded potential.

#### 2.1.1 Modeling evolution

We allow the galaxy potential to evolve with time by letting it track the dark matter halo growth using abundance matching (AM; Behroozi, Wechsler & Conroy 2013c). We enforce a constant offset in stellar mass at fixed halo mass such that the $z = 0$ galaxy mass matches the desired MW stellar disc mass at $z = 0$ for each of the simulations. Note that each halo has a different $z = 0$ virial mass (Table 2) and this means that each one has a different offset from the mean AM relation throughout its history. If it is low at $z = 0$, it is low at $z = 3$, and vice versa. However, while each galaxy/halo has a distinct growth rate, all of them end up the same observationally constrained ‘Milky Way’ galaxy at $z = 0$.

The scale radii at higher redshift are matched to median results from CANDELS, specifically those listed in Table 2 of van der Wel et al. (2014). The scale height is adjusted to keep the ratio between the scale length and height constant throughout time, with the $z = 0$ ratio as the chosen value. While this will keep the proportions of galaxy components constant, the overall size of the galaxy grows with time as informed by observations. The galaxy mass evolution for one of our hosts is shown in Fig. A1 for reference.

#### 2.1.2 Stellar disc

The stellar disc of most galaxies is well represented with an exponential form (Freeman 1970). However, the potential for such a distribution cannot be derived analytically. An alternative analytic potential commonly used is the Miyamoto & Nagai (1975, MN) disc potential:

$$\Phi(R, z) = \frac{GM_d}{\sqrt{R^2 + (R_d + \sqrt{z^2 + b^2})^2}}$$

where $M_d$ is the total disc mass, $R_d$ is the scale length, $b$ is the scale height, and $R$ and $z$ are the radial and vertical distances from the centre, respectively.

Unfortunately, a single MN disc is a poor match to an exponential disc. The surface density in the centre is too low and the surface density too high at large radii. A better approximation comes from the combination of three MN disc potentials (Smith et al. 2015). This technique matches an exponential disc within 2 percent out to 10 scale radii. We adopt the fits provided by Smith et al. (2015) and sum three MN discs together to model the exponential stellar disc with our chosen scale height and scale length.

#### 2.1.3 Gas disc

The gaseous disc is modeled as an exponential by implementing the same triple MN disc technique discussed above (Smith et al. 2015). The gas disc masses at high redshift are determined using the observational results of Popping et al. (2015), who provide gas...
Table 2. Discography of halo properties at $z = 0$. Haloes are listed in pairs corresponding to DMO (first) and those run with embedded galactic potentials (second, designated ‘Disc’). The remaining columns list the Bryan & Norman (1998) virial mass, virial radius, maximum circular velocity, $V_{\text{max}}$, and virial velocity ($\sqrt{GM_\text{vir}/R_\text{vir}}$), along with the total number of subhaloes with $V_{\text{max}} > 4.5 \text{ km s}^{-1}$ that survive to $z = 0$ within 25, 50, 100, and 300 kpc of the halo centre, the concentration based off a best-fitting NFW, and the redshift at which the host obtained 50 per cent of its final mass.

| Simulation        | $M_c$    | $R_c$   | $V_{\text{max}}$ | $V_v$     | $N_{\text{sub}} < 25$ kpc | $N_{\text{sub}} < 50$ kpc | $N_{\text{sub}} < 100$ kpc | $N_{\text{sub}} < 300$ kpc | $c_{\text{NFW}}$ | $z_{0.5}$ |
|-------------------|----------|---------|-------------------|-----------|--------------------------|---------------------------|-----------------------------|-----------------------------|----------------|----------|
| Hound Dog         | 1.95     | 330     | 192               | 160       | 118                      | 551                       | 1858                        | 6212                        | 10.02          | 1.14     |
| Hound Dog Disc    | 1.95     | 330     | 202               | 160       | 12                        | 213                       | 925                         | 4351                        | 11.82          | 1.31     |
| Blue Suede        | 1.74     | 317     | 196               | 154       | 48                        | 304                       | 1139                        | 4368                        | 12.36          | 0.74     |
| Blue Suede Disc   | 1.76     | 319     | 206               | 155       | 4                        | 106                       | 678                         | 3082                        | 14.23          | 0.76     |
| Teddy Bear        | 1.57     | 307     | 183               | 149       | 62                        | 411                       | 1562                        | 5138                        | 10.43          | 0.99     |
| Teddy Bear Disc   | 1.58     | 307     | 196               | 149       | 14                        | 130                       | 817                         | 3668                        | 11.78          | 1.05     |
| Las Vegas         | 1.35     | 292     | 175               | 142       | 65                        | 336                       | 1237                        | 4200                        | 11.21          | 0.83     |
| Las Vegas Disc    | 1.40     | 295     | 189               | 143       | 8                        | 104                       | 644                         | 2992                        | 13.48          | 0.86     |
| Jailhouse         | 1.17     | 278     | 170               | 135       | 71                        | 283                       | 965                         | 3384                        | 11.73          | 1.15     |
| Jailhouse Disc    | 1.20     | 280     | 188               | 136       | 13                        | 104                       | 486                         | 2555                        | 15.58          | 1.21     |
| Suspicious        | 1.08     | 271     | 158               | 131       | 60                        | 339                       | 1156                        | 3520                        | 9.58           | 0.96     |
| Suspicious Disc   | 1.10     | 272     | 166               | 132       | 10                        | 133                       | 666                         | 2639                        | 11.23          | 0.97     |
| Kentucky          | 1.09     | 271     | 183               | 132       | 75                        | 298                       | 899                         | 2791                        | 18.03          | 1.78     |
| Kentucky Disc     | 1.08     | 271     | 202               | 131       | 9                        | 85                        | 365                         | 1761                        | 24.15          | 2.22     |
| Lonesome          | 1.02     | 265     | 159               | 129       | 91                        | 378                       | 1154                        | 3390                        | 11.14          | 1.56     |
| Lonesome Disc     | 1.04     | 267     | 180               | 130       | 5                         | 121                       | 494                         | 2164                        | 16.54          | 1.55     |
| Tender            | 0.95     | 259     | 152               | 126       | 74                        | 344                       | 1070                        | 3190                        | 10.16          | 0.81     |
| Tender Disc       | 0.96     | 260     | 171               | 126       | 7                         | 97                        | 448                         | 2112                        | 16.05          | 0.84     |
| Hard Headed       | 0.85     | 250     | 160               | 121       | 97                        | 492                       | 1389                        | 3296                        | 14.54          | 1.79     |
| Hard Headed Disc  | 0.89     | 253     | 179               | 123       | 14                        | 175                       | 782                         | 2412                        | 18.65          | 1.76     |
| Shook Up          | 0.72     | 236     | 147               | 115       | 92                        | 346                       | 1007                        | 2740                        | 12.16          | 1.46     |
| Shook Up Disc     | 0.73     | 238     | 173               | 115       | 8                        | 138                       | 561                         | 1767                        | 20.67          | 1.51     |
| All Right         | 0.65     | 229     | 140               | 111       | 66                        | 328                       | 898                         | 2544                        | 12.02          | 1.69     |
| All Right Disc    | 0.71     | 235     | 164               | 114       | 5                         | 116                       | 479                         | 1765                        | 17.10          | 1.28     |

fractions, $f_g = M_{\text{gas}}/(M_{\text{gas}} + M_*)$, for galaxies as a function of stellar mass. Specifically, we use their median values for the cold gas fraction as a function of stellar mass and redshift to fit a 2D regression. We then use this fit along with the stellar disc mass and redshift to set the cold gas mass. The scale lengths of the gas disc are fixed to be the same constant ratio with the stellar disc given at $z = 0$.

2.1.4 Stellar bulge

The bulge is modeled as a Hernquist (1990) potential where the scale length is a constant multiple of the stellar scale length as determined by both components’ scale lengths at $z = 0$. The bulge mass evolves to maintain the same ratio of bulge mass to stellar mass present at $z = 0$.

3 RESULTS

Fig. 1 shows example visualizations of the dark matter distribution for a typical halo in our suite simulated without (left) and with (right) the galaxy potential. This is the halo identified as ‘Kentucky’ and ‘Kentucky Disc’ in Table 2. The top panels are 500 kpc boxes and correspond approximately the virial volume of this halo (with $R_e \approx 270$ kpc). The lower panel is zoomed in to a region 100 kpc across. Qualitatively, our results are very similar to those of Garrison-Kimmel et al. (2017b). The presence of a central galaxy eliminates a majority of the substructure in the innermost region ($\leq 50$ kpc) but has only a minimal effect at large radius. The notable enhancement of dark matter, seen in the very centre of the DMO run, is due to baryonic contraction. This effect is also apparent in full hydrodynamic simulations at this mass scale (Garrison-Kimmel et al. 2017a).

3.1 Velocity functions

Fig. 2 shows the velocity functions for subhaloes in the DMO (black) and disc simulations (magenta). Shown are cumulative $V_{\text{max}}$ distributions (left columns) and $V_{\text{peak}}$ distributions (right column) of all the resolved subhaloes within 300, 100, and 50 kpc in top, middle, and bottom rows, respectively. The bands bound the minimum and maximum values for each velocity bin and the thick lines represent the medians. The inclusion of a central galaxy potential (magenta) to the DMO runs affects subhaloes of all masses roughly uniformly and has a greater impact on the total number of subhaloes in regions closer to the disc. Within 300 kpc, the Disc runs have $\sim 70$ per cent of the number of subhaloes seen in the DMO runs, roughly independent of velocity. At 100 kpc, the offset is close to a factor of $\sim 2$. Within 50 kpc, the difference is close to a factor of $\sim 3$.

One important feature seen in Fig. 2 is the roll-off in the $V_{\text{peak}}$ functions at small velocity. This is both a sign and a measure of incompleteness. Incompleteness in $V_{\text{peak}}$ gets worse at smaller...
Figure 1. Visualization of the dark matter for Kentucky (left) and Kentucky Disc (right). The top panels span 500 kpc, approximately the virial volume of this halo. The bottom panels span 100 kpc. The absence of substructure at small radii in the Disc runs is striking. An enhancement in central dark matter density is also seen in the Disc runs, which is a result of baryonic contraction. The disc potentials are oriented face-on in these images.

radius (where stripping is more important) as might be expected. Within 100 kpc (middle right) we show signs of incompleteness below $V_{\text{peak}} \approx 5 \text{ km s}^{-1}$. Within $R = 50$ kpc (bottom right) we appear complete for $V_{\text{peak}} > 6 \text{ km s}^{-1}$. Note that we show no major signs of completeness issues down to $V_{\text{max}} = 4.5 \text{ km s}^{-1}$ for all radii we have explored. In Appendix A we present a resolution test using re-simulations of a DMO and Disc run with 64 times worse mass resolution. Scaling from $V_{\text{max}} = 4.5 \text{ km s}^{-1}$ to the lower resolution simulation, we would expect convergence down to $V_{\text{max}} \simeq 15 \text{ km s}^{-1}$ (following the mass trend for subhalos, $M \propto V_{\text{max}}^{3.45}$). We indeed find agreement with the higher resolution simulation at $V_{\text{max}} = 15 \text{ km s}^{-1}$ in both the DMO and Disc resimulations.

3.2 Radial distributions

As seen in Fig. 2, the difference between the DMO and Disc runs increases with decreasing distance from the halo centre. This point is emphasized in Fig. 3, which shows cumulative radial profiles at fixed $V_{\text{max}}$ (left) and $V_{\text{peak}}$ (right) cuts in both DMO and Disc runs.

The left-hand panel of Fig. 3 shows the cumulative radial count of subhaloes with $V_{\text{max}} > 4.5 \text{ km s}^{-1}$ for each of our 12 DMO (black dash) and Disc (magenta) hosts. The thick black lines show medians for each of the distributions. Note that while the difference in overall count is only ~30 per cent out at 300 kpc, the offset between DMO and Disc grows to more than an order of magnitude at small radius, and is typically a factor of ~20 at $R = 25$ kpc. The
Figure 2. Cumulative $V_{\text{max}}$ (left) and $V_{\text{peak}}$ (right) distributions for subhaloes within $R = 300$, 100, and 50 kpc (top to bottom) for all 12 of our DMO (black) and DMO+Disc runs (magenta). The solid lines are medians, while the shaded bands span the full extent of the distributions. Note that the roll-offs at low $V_{\text{peak}}$ in the right-hand panels are signatures of incompleteness. The $V_{\text{peak}}$ completeness limit gets worse as we approach the halo centres (where stripping is more important). The simulations appear reasonably complete to $V_{\text{peak}} \approx 5\text{ km s}^{-1}$ within 300 kpc. This limit drops to $V_{\text{peak}} \approx 6\text{ km s}^{-1}$ within 50 kpc. There is no such roll-off in $V_{\text{max}}$, which suggests that we are complete down to $V_{\text{max}} \approx 4.5\text{ km s}^{-1}$ throughout the haloes.

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Figure 3. Cumulative counts for subhaloes within a given radius of the host. The black dashed lines represent the dark matter-only runs and the magenta lines represent the same haloes with an embedded MW-like potential. Left: subhaloes with $V_{\text{max}} > 4.5\, \text{km s}^{-1}$. Right: subhaloes with $V_{\text{peak}} > 10\, \text{km s}^{-1}$. Note that the vertical axis scales are significantly different on the left and right.

majority of the $\text{Disc}$ runs have no identifiable substructure within 20 kpc. None of the $\text{Disc}$ simulations have even a single subhalo within 10 kpc. As can be seen in Table 2, the systematic depletion of central subhaloes occurs in every host, including the most massive halo (Hound Dog), where the ratio of galaxy mass to halo mass is the smallest.

The right-hand panel of Fig. 3 tells a similar story. Here we have chosen a fairly large cut in $V_{\text{peak}} > 10\, \text{km s}^{-1}$. This scale is similar to, though somewhat smaller than, the natural scale where galaxy formation might naively be suppressed by an ionizing background (e.g. Okamoto et al. 2008). The majority of the $\text{Disc}$ runs have nothing with $V_{\text{peak}} > 10\, \text{km s}^{-1}$ within $\sim 30$ kpc. As discussed in Section 4.1 and in Graus et al. (2018a), the fact that we already know of five Milky Way satellites within 30 kpc of the Galactic centre (and that we are not complete to ultra-faint galaxies over the full sky) suggests that we may need to populate haloes well smaller than this ‘natural’ scale of galaxy formation in order to explain the satellite galaxy population.

3.3 Pericentre distributions

At first glance, it is potentially surprising that the existence of a galaxy potential confined to the central regions of a halo can have such a dramatic effect on subhalo counts at distances out to $\sim 100$ kpc. As first discussed by Garrison-Kimmel et al. (2017b), the pericentre\(^4\) distribution of subhaloes provides some insight into this question.

Fig. 4 shows the pericentre distributions of all subhaloes found within $R = 100$ kpc at $z = 0$ in both the DMO (dashed) and $\text{Disc}$ runs (solid). There is a unique (thin) line for each halo, colour coded by the halo virial mass (colour bar). The thick black lines are medians. While the two distributions are similar for large pericentre differences ($R \gtrsim 40$ kpc) the differences are dramatic at $R \lesssim 20$ kpc. Subhaloes in the DMO simulations exist on quite radial orbits, with $d_{\text{peri}}$ distributions that spike towards $d_{\text{peri}} = 0$. Surviving subhaloes in the $\text{Disc}$ runs, on the other hand, have distributions that peak at $d_{\text{peri}} \sim 35$ kpc and have a sharp decline towards $d_{\text{peri}} = 0$. It is clear that subhaloes that get close to the galaxy potentials are getting destroyed.

\(^4\)Pericentres were obtained by interpolating the subhalo positions between snapshots and storing the minimum separation between the host and the subhalo as the pericentre. The time between interpolated snapshots is 14–16 Myr.
Fig. 4 also shows that the differential effect of the disc potential on a given halo varies dramatically based on the underlying orbital distribution of its subhaloes. DMO haloes that have the largest spike in low pericentres will have the largest overall shift in subhalo counts once disc potentials are included. We find that for subhaloes that exist within 300 kpc but have never passed within 20 kpc, the difference in the radial and orbital distributions between the DMO and Disc runs is negligible.

### 3.4 Infall times

The subhaloes that are present in the DMO runs but absent in the Disc runs are biased not only in their orbital properties (Fig. 4) but in the time they have spent orbiting within their host haloes. Fig. 5 shows the infall time distributions for subhaloes with $V_{\text{max}} > 4.5 \text{ km s}^{-1}$ for all of the DMO simulations (gray) and for the Disc re-runs (magenta). The left-hand panel shows infall times for subhaloes that exist within 300 kpc of their host halo centres at $z = 0$. The right-hand panel shows infall times for subhaloes within 100 kpc. Times are plotted as lookback ages, with zero corresponding to the present day.

Both panels of Fig. 5 clearly demonstrate that subhaloes with early infall times are preferentially depleted in the Disc runs. The differences are particularly significant for infall times greater than 6 Gyr ago: the early-infall tails are considerably depressed in the Disc. Interestingly, the shifts in median lookback times to infall are modest as we go from DMO to Disc: 7.6–6.1 Gyr in the 300 kpc panel and 8–6 Gyr in the 100 kpc panel. Also, the Disc simulations show a slight enhancement of late-time accretions ($\sim 1$–2 Gyr). This may be related to the halo contraction that occurs as the galaxy grows at late times (see concentration comparison in Table 2). It is possible that some subhaloes enter the viral volume faster than they would in the DMO equivalent because of this effect. More analysis will be needed to test this hypothesis because the halo virial mass itself shows no such enhancement at late times.

### 3.5 Time evolution of substructure counts

Substructure in dark matter haloes is set by a competition between the accretion rate of small haloes and the mass-loss rate from dynamical effects over time (e.g. Zentner & Bullock 2003). A central galaxy potential increases the destruction rate, which depletes subhalo populations compared to DMO simulations.

One question is whether and to what extent differences in subhalo counts seen between DMO and Disc runs persist at earlier times. This may have important observational implications for substructure probes that are sensitive properties at early times. Cold stellar streams, for example, may have existed for multiple orbital times ($t_{\text{orb}} \sim 500 \text{ Myr}$). If the substructure population was significantly higher in the past and then this could manifest itself in observables today.

Fig. 6 explores this question by showing the count of $V_{\text{max}} > 4.5 \text{ km s}^{-1}$ subhaloes within a physical radius of 20 kpc of each halo centre as a function of lookback time. The bands show the full distributions over all simulations, with grey corresponding to DMO and magenta corresponding to the Disc runs. Solid lines are medians. We see that the overall offset between DMO and Disc runs persists to lookback times of 8 Gyr, but that for times prior to $\sim 4 \text{ Gyr}$ ago, the subhalo counts in the Disc runs begin to approach the DMO counts. In the median, the difference is ‘only’ a factor of $\sim 3$ eight billion years ago, compared to more than a factor of $\sim 30$ suppression at late times.

Overall, it appears that the expected suppression is quite significant in its implications for cold stellar stream heating. The median count of subhaloes in the Disc runs remains near zero over the past $\sim 2 \text{ Gyr}$ (compared to $\sim 50$ subhaloes in the DMO runs). This time-scale is $> 3$ orbital times for a cold stream like Pal-5 at $R = 20 \text{ kpc}$ and $V_{\text{orb}} \sim 200 \text{ km s}^{-1}$. The median subhalo count in the Disc runs remains less than 10 to lookback times of 4 Gyr. Cold streams that have persisted for more than 4 Gyr or extend out to $\sim 50 \text{ kpc}$ from the Galaxy may be required in order to provide robust probes of substructure, though a full exploration of this question will require further analysis.

Figure 5. Distributions of infall times when subhaloes first crossed into the host virial radius. Shown are distributions for all surviving subhaloes with $V_{\text{max}} > 4.5 \text{ km s}^{-1}$ within $R = 300 \text{ kpc}$ (left) and $R = 100 \text{ kpc}$ (right) stacked together for all of the DMO (gray) and Disc (magenta) simulations in our suite. The Disc runs are clearly depleted in subhaloes that fell in more than $\sim 6 \text{ Gyr}$ ago compared to the DMO runs, and especially so in the $R < 100 \text{ kpc}$ sample.
work well beyond that presented in this introductory paper. We hope that the public release of our subhalo catalogues will facilitate efforts of this kind.

4 IMPLICATIONS

4.1 What haloes host ultra-faint galaxies?

As alluded to in Section 3.2, the absence of substructure within the vicinity of the central galaxy in the Disc runs may have important implications for our understanding of the mapping between galaxy haloes and stellar mass. In particular, the relatively large number of galaxies that are known to exist within $\sim 50$ kpc of the Galactic centre provides important information about the lowest mass dark matter haloes that are capable of forming stars (Jethwa et al. 2018).

The majority of efforts to understand how the ionizing background suppresses galaxy formation have found that most dark matter haloes with $V_{\text{peak}} < 20$ km s$^{-1}$ are devoid of stars (e.g. Thoul & Weinberg 1996; Okamoto et al. 2008; Ocvirk et al. 2016; Fitts et al. 2017). A second scale of relevance for low-mass galaxy formation is the atomic hydrogen cooling limit at $10^4$ K, which corresponds to a $V_{\text{peak}} \simeq 16$ km s$^{-1}$ halo. Systems smaller than this would require molecular cooling to form stars. Taken together, one might expect that most ultra-faint satellite galaxies of the Milky Way should reside within subhaloes that fell in with peak circular velocities in the range $16 - 20$ km s$^{-1}$.

Compare this basic expectation to the information summarized in Fig. 7. Here we plot the median cumulative radial count of subhaloes with $V_{\text{peak}}$ values larger than a given threshold as derived from the full sample of Disc runs. The colour bar on the right indicates the $V_{\text{peak}}$ threshold and the solid lines track characteristic $V_{\text{peak}}$ values ($7, 10, 15, \text{and} 20$ km s$^{-1}$) as labeled. A similar figure that utilizes data from the DMO simulations is provided in Fig. 8.

Figure 7. Median cumulative radial counts of subhalos for all of the Disc runs color coded by $V_{\text{peak}}$ threshold. The faint gray lines mark $V_{\text{peak}}$ thresholds larger than $7, 10, 15, \text{and} 20$ km s$^{-1}$, respectively. Thick lines represent the Milky Way satellite data uncorrected (red dashed) and corrected for sky coverage (solid black). The vertical dotted line at 40 kpc represents an estimate of the radial completeness limit for $L \simeq 1000 L_\odot$ ultra-faint dwarfs. Observed counts to the right of this line should be treated as lower limits, as the true counts may be much higher than those shown given the lack of a deep, full sky survey. If our host halos are representative of the Milky Way, then we must populate all subhaloes with $V_{\text{peak}} \gtrsim 7$ km s$^{-1}$ in order to account for the data. This extrapolates to an implied total of $\sim 1000$ ultra-faint satellites within 300 kpc.

Figure 8. Median radial profiles for different $V_{\text{peak}}$ cuts for all of the DMO runs. Compare to the Disc simulations shown in Fig. 7. The faint gray lines represent the DMO data for fixed $V_{\text{peak}}$ thresholds of $7, 10, 15, \text{and} 20$ km s$^{-1}$, respectively. The thick lines represent the Milky Way satellite data uncorrected (red dashed) and corrected for sky coverage (solid black). Haloes with $V_{\text{peak}} \gtrsim 12$ km s$^{-1}$ are required to match the inner data in the median of our DMO runs, and this extrapolates to an implied total of $\sim 200$ ultra-faint satellites within 300 kpc.
The dashed red line shows the census\(^5\) of known MW satellites galaxies as compiled by Fritz et al. (2018). The thick black line in Fig. 7 applies a sky-coverage correction to derive a conservative estimate of the radial count of satellite galaxies. This correction assumes that 50 percent of the sky has been covered by digital sky surveys to the depth necessary to discover ultra-faint galaxies and adds a second galaxy for every MW dwarf known that has an absolute magnitude fainter than \(-6\). Importantly, even in the region of the sky that has been covered by digital sky surveys like SDSS and DES, our census of the faintest ultra-faint galaxies \((L \lesssim 10^3 L_\odot)\) is not complete at radii larger than \(\sim 40\) kpc (Walsh, Willman & Jerjen 2009). We draw attention to this fact with the vertical dotted line.

If our simulation suite is indicative of the Milky Way, we must associate the galaxies within 30 kpc with subhaloes that had maximum circular velocities at infall greater than just \(7\) km s\(^{-1}\) (corresponding to a peak infall mass of \(M_{\text{peak}} \simeq 3 \times 10^7 M_\odot\); Garrison-Kimmel et al. 2014). This is not only well below the canonical photo-ionization suppression threshold (\(\sim 20\) km s\(^{-1}\)), it is smaller than the atomic cooling limit (\(\sim 16\) km s\(^{-1}\)). The virial temperature of the required \(\sim 7\) km s\(^{-1}\) halo is 2000 K, which likely would need efficient molecular cooling for star formation to proceed. If we perform the same exercise host-by-host, the minimum \(V_{\text{peak}}\) required to explain the galaxy counts within 40 kpc varies some. Nine of our 12 Disc runs require \(V_{\text{peak}} = 6.5\)−7.5 km s\(^{-1}\) to explain the counts within 40 kpc. The other three require \(V_{\text{peak}} = 8.1, 9.2,\) and 9.3 km s\(^{-1}\), respectively. We find no trend between the minimum \(V_{\text{peak}}\) required to explain the known counts and host halo mass. In a companion paper by Graus et al. (2018a), we explore the implications of this basic finding and provide a statistical comparison based on each of our Disc runs individually.

In addition to changing our basic picture of low-mass galaxy formation, the need to populate tiny haloes is rare in MW-size hosts and we are focusing primarily on implications for ultra-faint satellites.

\(^5\)The Fritz et al. (2018) compilation does not include the LMC and SMC. We also exclude their presence here to be conservative, as massive subhalos of this kind are rare in MW-size hosts and we are focusing primarily on implications for ultra-faint satellites.

### 4.2 Satellite pericentres

As we discussed in reference to Fig. 4, subhalo pericentre distributions are dramatically different once the galaxy potential is included. Here we take advantage of recent insights on satellite galaxy orbits made possible by Gaia to determine which of these distributions is more in line with observations (Erkal et al. 2018; Fritz et al. 2018; Gaia Collaboration 2018; Pace & Li 2018, Simon 2018).

Fig. 9 presents a comparison of subhalo pericentres in the DMO (dashed) and Disc runs (solid) to those of MW satellite galaxies. Shown in red are the differential (left) and cumulative (right) pericentre distributions of MW galaxies from Fritz et al. (2018) that have \(z = 0\) distances within 100 kpc of the Galactic centre. The Fritz et al. (2018) sample includes proper motions of 21 satellite galaxies within 100 kpc. Two MW potentials are used in Fritz et al. (2018) to derive the pericentre distances of each satellite. They are based on the MWPotential\(^4\) potential (see Bovy 2015 for details) with a light and heavy DM halo with virial masses of \(0.8 \times 10^{12} M_\odot\) and \(1.6 \times 10^{12} M_\odot\), respectively. For clarity, we only include the results of the ‘Light’ MW potential, which is closer to the median halo mass of our sample \((1.1 \times 10^{12} M_\odot)\). Results for the ‘Heavy’ MW potential are very similar and can be found in Appendix A.

In order to fairly compare predictions to observations in this space, we must account for observational incompleteness. Our current census of faint galaxies is radially biased within 100 kpc, such that we are missing galaxies at large radii. In order to make a fair comparison, we took all subhaloes with \(V_{\text{max}} > 4.5\) km s\(^{-1}\) within a \(z = 0\) distance of 100 kpc of the centre of each halo and then subsampled those populations 1000 times for each halo to create present-day radial distributions that match those of the satellites in Fritz et al. (2018). We then ‘stacked’ these populations together to derive median pericentre distributions for subhaloes in each of the two classes of simulations (DMO and Disc). Note that each host halo is equally weighted.

The left-hand panel of Fig. 9 compares the median of the radially re-sampled distributions to the distribution of pericentres derived by Fritz et al. (2018). As foreshadowed in Fig. 4, the DMO subhaloes have a pericentre distribution that spikes towards small values, very unlike the distribution seen in the real data. The Disc runs, on the other hand, show a peak at \(\sim 30\) kpc with rapid fall-off at smaller radii and a more gradually fall-off towards larger distances. This shape is quite similar to that seen in the real data. Note that if we choose subhaloes with \(V_{\text{peak}} > 7\) km s\(^{-1}\) instead, the distributions are almost indistinguishable (see Appendix A). It is interesting that the total lack of subhaloes with pericentres smaller than 20 kpc is not seen in the data. The two galaxies in this inner bin are Segue 2 and Tucana III; these systems may very well be in the process of disruption.

In the right-hand panel of Fig. 9 we present the same data cumulatively and also explore how uncertainties in the derived orbits affect the comparison. Specifically, we used the quoted errors given by Fritz et al. (2018) on each galaxy and drew from a Gaussian to generate 10,000 realizations for each system. The median of the resultant distribution is given by the thick red line with 95 per cent confidence intervals shown by the shaded band. The DMO distribution is well above the 95 per cent region everywhere within 50 kpc. The median of Disc runs remains within the spread for all but the inner most region.

From the above comparison, we conclude that the DMO runs produce a pericentre distribution for satellite subhaloes that is quite far from what is observed for Milky Way satellite galaxies. The Disc runs are much closer to what is observed and therefore appear to provide a more realistic comparison set. The clear next step in
this comparison is to re-derive the implied pericentre distributions for each host halo’s mass and to directly compare predictions in full phase space to those observed. While such an analysis is beyond the scope of this introductory paper, future work in this direction is warranted. Understanding how host halo-to-halo scatter, ongoing satellite disruption, and specifics of halo finding affect these interpretations will also be important.

5 DISCUSSION AND CONCLUSIONS

In this paper, we have introduced Phat ELVIS suite of 12 high-resolution simulations of Milky Way mass dark matter haloes that are each run with (Disc) and without (DMO) a Milky Way disc galaxy potential. As summarized in Table 2, the host halo masses in our suite span \( M_{\text{vir}} = (0.7 - 2) \times 10^{12} \, M_\odot \), which encompasses most recent estimates for the virial mass of the Milky Way (Bland-Hawthorn & Gerhard 2016). The galaxy potential at \( z = 0 \) is the same for each Disc run and is summarized in Table 1. As demonstrated in Fig. 2, our resolution allows us to have convergence in identifying subhaloes down to a maximum circular velocity of \( V_{\text{max}} = 4.5 \, \text{km s}^{-1} \) (\( M \approx 5 \times 10^6 \, M_\odot \)) and with peak (infall) circular velocities \( V_{\text{peak}} \approx 6 \, \text{km s}^{-1} \) (\( M_{\text{peak}} \approx 1.8 \times 10^7 \, M_\odot \)). The main effect of the Milky Way potential on subhalo populations is that subhaloes with pericenters smaller than \( \sim 20 \, \text{kpc} \) are depleted in the Disc runs (see Fig. 4).

5.1 Impact of the disc on substructure populations

The most striking difference between the Disc and DMO subhaloes is in their abundances at radii smaller than \( \sim 50 \, \text{kpc} \) at \( z = 0 \). This difference can be seen visually in Fig. 1 and quantitatively in Fig. 3. Table 2 lists counts as a function of various radial choices and shows that the ratio of subhalo counts between the Disc to DMO runs at \( z = 0 \) is typically \( \sim 1/10 \) at \( R < 25 \, \text{kpc} \), \( \sim 1/3 \) at \( R < 50 \, \text{kpc} \), and \( \sim 1/2 \) at \( R < 100 \, \text{kpc} \). Note that these ratios are fairly constant independent of the host halo virial radius (or concentration). To zeroth order, the depletion radius appears to be set by the disc potential (which is the same for all runs), not host halo properties. The most important predictor for relative depletion seems to be the variable pericentre distributions in the DMO runs: simulations that have subhaloes with an overabundance of pericenters smaller than \( \sim 20 \, \text{kpc} \) will experience more relative depletion once the galaxy potential is included.

Another difference between the surviving subhalo populations in the DMO and Disc runs is in the distribution of infall times (see Fig. 5). If the galaxy potential is included, the majority of subhaloes that fell in more than \( \sim 8 \, \text{Gyr} \) ago and survived in the DMO runs become destroyed in the Disc runs. This may have important implications for models of environmental galaxy quenching when applied to the Milky Way (Wheeler et al. 2014; Fillingham et al. 2015; Wetzel, Tollerud & Weisz 2015; Rodriguez-Wilberly et al. 2018) and may also potentially change the expected mapping between orbital energies and infall time expected for Milky Way satellites (Rocha, Peter & Bullock 2012).

5.2 Numerical convergence

Before moving on to summarize some potential observational implications of our results, it is worth discussing numerical completeness. Fig. 2 provides evidence that the mass functions are converged for subhaloes with infall masses down to \( M_{\text{peak}} \approx 1.8 \times 10^7 \, M_\odot \) (\( N_p \approx 600 \) particles). This level of completeness is typical of that quoted for simulations of this kind (e.g. Springel et al. 2008; Garrison-Kimmel et al. 2014). In Appendix A we present a resolution test using a re-simulation of one of our haloes with 64 times worse mass resolution, and show that we are indeed
converged to subhalos that are 64 times more massive than we have estimated in the high-resolution runs. We also show using this low-resolution comparison that there is not a significant difference in convergence between the DMO and Disc runs. This suggests that the offset between our Disc and DMO subhalo distributions is a real, physical effect.

While we have shown convergence, it is important to remind ourselves that convergence to an answer does not necessarily imply convergence to the correct answer. Such a concern is raised by van den Bosch et al. (2018) and van den Bosch & Ogiya (2018), who have performed numerical experiments showing that many more particles may be required for robust tracking of subhalo disruption. For example, van den Bosch et al. (2018) find that orbits passing within 20–20 per cent of the virial radius of a host (30–60 kpc for our haloes) may require Np > 10^6 particles for an accurate treatment. For our simulations, this would correspond to subhaloes with mass \( \sim 3 \times 10^6 M_\odot \) or \( v_{\text{max}} \sim 30 \text{ km s}^{-1} \). As can be seen in Fig. 2, even at this mass scale our simulations still show significant differences between the DMO and Disc runs at small radius, and at roughly the same ratios reported for the lower-mass regime. More work will be required to understand the origin of the puzzling differences between our naive understanding of convergence and the detailed work by van den Bosch & Ogiya (2018) to thoroughly understand subhalo mass-loss.

### 5.3 Observable consequences

Modulo the above concerns about potential completeness issues, the simulation suite presented here has produced a number of results with potentially interesting implications for interpreting observations.

(i) The majority of the Disc simulations have no subhaloes larger than \( v_{\text{max}} = 4.5 \text{ km s}^{-1} \) within 20 kpc (Fig. 3) and the overall count of subhaloes within this radius remains depressed compared to the DMO runs for several billion years in the past (Fig. 6). This suggests that local stream-heating signals from dark substructure may be quite rare, even in cold dark matter models without suppressed small-scale power spectra.

(ii) The pericentre distributions of Milky Way satellites derived from Gaia data are remarkably similar to the pericentre distributions of subhaloes in the Disc runs, while the DMO runs drastically overpredict galaxies with pericentres smaller than 20 kpc (Fig. 9). This suggests that the Galaxy potential must be considered in any attempt to understand the dynamics and evolution of Milky Way satellites, especially those that exist within the inner \( \sim 100 \text{ kpc} \) of the Milky Way.

(iii) As shown in Fig. 7, the depletion of inner substructure in the Disc runs presents a tension with satellite galaxy counts that is in the opposite sense as that in the Missing Satellites Problem. In order to account for all of the ultra-faint galaxies known within 40 kpc of the Galaxy, we must populate haloes well below the atomic cooling limit (\( v_{\text{peak}} \sim 7 \text{ km s}^{-1} \) or \( M \sim 3 \times 10^7 M_\odot \) at infall). The precise value for the minimum \( v_{\text{peak}} \) varies from host to host, with 9 of our 12 Disc runs requiring \( v_{\text{peak}} = 6.5–7.5 \text{ km s}^{-1} \) to explain the counts within 40 kpc. The other three require \( v_{\text{peak}} = 8.1, 9.2, \) and \( 9.3 \text{ km s}^{-1} \), respectively. There is no apparent trend with host halo mass in the derived minimum values. This issue is discussed in more detail in a companion paper by Graus et al. (2018a).

(iv) If tiny \( v_{\text{peak}} \sim 7 \text{ km s}^{-1} \) haloes do host ultra-faint galaxies, as implied by Fig. 7, this implies the existence of at least \( \sim 1000 \) satellite galaxies within 300 kpc of the Milky Way. The number density of such tiny haloes is \( \sim 100 \text{ Mpc}^{-3} \) (e.g. Bullock & Boylan-Kolchin 2017) in the field, suggesting that there may be \( \sim 100,000 \) ultra-faint galaxies for every L* galaxy in the universe.

The aim of this simulation suite is to provide a more accurate set of predictions for dark subhalo properties by including the inevitable existence of a central galaxy potential in calculations of their dynamical evolution. We have focused here on a Milky Way galaxy analogue in order to make direct connections to the well-studied population of Milky Way satellites. A similar approach could be used to model satellite subhalo populations for a diverse set of galaxies.

We have shown that the presence of the galaxy significantly changes our expectations for subhalo counts, orbits, and dynamical evolution and that this has a direct bearing on our interpretation of observed satellite galaxy properties as well as efforts to find dark subhalos. Future work in this direction may prove vital in efforts to constrain the nature of dark matter and the physics of galaxy formation on the smallest scales.

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APPENDIX A: SUPPLEMENTARY INFORMATION

Fig. A1 provides an example growth history for Kentucky in order to illustrate how our galaxy components are evolved. The dashed black line shows the main progenitor halo growth. The solid black line shows the growth of the full galaxy mass. The stellar disc (blue dashed), gas disc (red dotted), and bulge (green dash-dot) are forced to the values listed in Table 1 at z = 0. The stellar mass (disc plus bulge) is set to track the host halo growth using abundance matching. The gas disc masses at high redshift are determined using the observational results of Popping et al. (2015), who provide gas fractions for galaxies as a function of stellar mass.

Fig. A2 is analogous to Fig. 9 in that it compares the pericentre distributions of subhaloes to those of Milky Way satellite galaxies presented in Fritz et al. (2018). Here we include the pericentres derived using both the ‘Light’ (red) and ‘Heavy’ (blue) MW potential in Fritz et al. (2018). We also show the subhalo distributions for a $V_{\text{max}}$ cut ($> 4.5 \text{ km s}^{-1}$, left) and $V_{\text{peak}}$ cut ($> 7 \text{ km s}^{-1}$, left).
Figure A1. Mass growth of the galaxy for Kentucky with scale factor. The individual components’ growths as well as the total galaxy mass growth. The final ($a = 1$) position of all galaxy lines (not the dark matter halo virial mass) is fixed for all hosts as discussed in Section 2.1. The dashed line near the top of the figure shows the halo’s virial mass evolution.

Figure A2. Differential pericentre distributions for subhaloes (black) with $V_{\text{max}} > 4.5 \text{ km s}^{-1}$ (left) and $V_{\text{peak}} > 7 \text{ km s}^{-1}$ (right) and MW satellites derived from both potentials used in Fritz et al. (2018). The pericentres derived using the ‘Light’ MW potential are shown by the red line and is the same as Fig. 4 while those derived using the ‘Heavy’ MW potential are shown by the blue line. The gray bands represent the 95 per cent confidence interval for the subhaloes’ distributions.

Figure A3 illustrates the effects of numerical resolution on the $V_{\text{max}}$ function for the ‘Hound Dog’ host halo. The black line shows the results obtained from our fiducial resolution for all objects within 50 kpc (left panel) and 300 kpc (right panel). The red line shows the results obtained from the same halo rerun with 64 × fewer particles. The estimated completeness for our high-resolution runs used in the main paper is $V_{\text{max}} = 4.5 \text{ km s}^{-1}$ (corresponding to subhalos with ~170 particles; see Section 3.1). Using $M \propto V_{\text{max}}^{3.45}$, we would expect the lower resolution comparison to be complete to $V_{\text{max}} \approx 15 \text{ km s}^{-1}$ at fixed particle count. We note that the two simulations do indeed begin to systematically differ only below $V_{\text{max}} \approx 15 \text{ km s}^{-1}$, which is indicated by the vertical dotted line. Fig. A4 shows the radial distributions of subhaloes with $V_{\text{max}} > 15 \text{ km s}^{-1}$ from our high-resolution and low-resolution runs both with (dashed) and without (solid) embedded galaxy potentials. The two resolutions are consistent to within counting errors at all radii. Importantly, the DMO and Disc runs appear to be converged down to the same $V_{\text{max}}$, which suggests that the differences we see with and without the galaxy potential are real, physical differences and not associated with spurious numerical effects.
Figure A3. Comparison of the subhalo counts of the Hound Dog host halo from our fiducial (high, black) run to a lower resolution run (low, red), with $64 \times$ fewer particles. The left-hand panel shows a cumulative count of all subhaloes above a given $V_{\text{max}}$, within 50 kpc of the host centre. The right-hand panel is similar but includes subhaloes out to 300 kpc. The vertical dotted line indicates where we would expect convergence ($V_{\text{max}} = 15 \text{ km s}^{-1}$) by scaling our adopted completeness threshold for the fiducial high-resolution runs ($V_{\text{max}} = 4.5 \text{ km s}^{-1}$).

Figure A4. Radial radial distributions of subhaloes with $V_{\text{max}} > 15 \text{ km s}^{-1}$ for the Hound Dog host halo from the fiducial resolution (high, black) and a run with $64 \times$ fewer particles (low, red). Runs with Milky Way potentials \texttt{Disc} are shown as the dashed lines. The counts agree to within expected Poisson variation for both types of runs at all radii.

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