Optimisation of the Q Factor of a Complementary Frequency Selective Surface

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Abstract

The complementary frequency selective surface (CFSS) consists of an array of dipoles and slots either side of a thin dielectric and exhibits a sharp passband. The conductors layer adds capacitance to the apertures layer which in turn miniaturises the FSS. In this paper, the CFSS is placed in a waveguide and the Q factor is maximised by varying the electric properties and physical parameters. The fabricated CFSS structure shows good agreement with the simulations.

1 Introduction

Frequency selective surfaces (FSS) have been studied for many years. Slots in a metal sheet behave as band-pass filters while unconnected metal elements act as band-stop filters [1]. The theory, analysis and design of FSS were described in [2] and [3]. In recent studies [4] and [5], the FSS structure was used as the resonator device in the waveguide for dielectric permittivity measurements. Moreover, a concept of the CFSS was first introduced in [6] as a hybrid of two closely coupled FSS in which a layer of conducting elements and a layer of aperture elements are etched either side of a thin dielectric substrate. The schematic representation of CFSS structure is shown in Figure 1. The CFSS structure is advantageous compared to conventional FSS structure due to having a highly stable passband with angle of incidence [6], [7] and being miniaturised due to the extra capacitance [8]. Additional CFSS studies were also conducted in [9]–[11]. As a result of studies [8], [11], the CFSS structure has the potential capability to be used for dielectric property measurements by observing the shift in resonant frequency. Therefore, an accurate and precise determination of the measured resonant frequency becomes critical. In order to accurately measure the change in the measured resonant frequency, the Q factor of the CFSS should be maximised. In this paper, the physical and dielectric parameters of the CFSS structure were studied. Based on this analysis an optimised CFSS structure was designed using real materials.

2 Method

The CFSS structure was deployed inside an X-band waveguide. The X-band waveguide frequency range was from 8.2 to 12.4 GHz, and the size was 22.86 mm × 10.16 mm. The width and height of the CFSS structure were designed to fit in the X-band waveguide and were 22.86 mm and 10.16 mm, respectively. The conductors and the apertures layer were copper. The simulations were conducted using Empire XPU commercial electromagnetic software. In the simulations, unless the designated parameter was studied, the common data used were: conductors length ($l_c$) = 2.5 mm; conductors width ($w_c$) = 0.5 mm; conductors layer thickness ($t_c$) = 0.017 mm; apertures length ($l_a$) = 2.5 mm; apertures width ($w_a$) = 0.5 mm; apertures layer thickness ($t_a$) = 0.017 mm; in-between substrate: relative permittivity ($\varepsilon_{is}$) = 4; loss tangent (tan$\delta_{is}$) = 0.01 and thickness ($d_{is}$) = 0.05 mm.

3 Parameter Optimisation

The CFSS structure consisted of three parts: conductors layer, in-between substrate and apertures layer. Note, in this section the dimensions of the apertures and conductors were varied independently.
3.1 Conductors Layer

The conductors layer are inherently a band-stop filter. When the conductor is larger, the Q factor of the CFSS is higher. Therefore, as either the length or the width of the conductor increased, the Q factor increased. When the conductor length was increased from 2.5 mm to 3.5 mm, the Q factor increased by 13%. Meanwhile, as the width was increased from 0.5 mm to 1.5 mm, the Q factor increased by 3%. The thickness of the conductors layer was also considered and the result show the Q factor slightly decreased when the thickness increased. The three parameter results for the conductors layer are shown in Figure 2.

3.2 Apertures Layer

In contrast to the conductors layer, the apertures layer acts as a band-pass filter. When the aperture was larger, the Q factor of the CFSS was reduced. As the length or the width of the aperture was increased, the Q factor decreased as expected. When the length increased from 2.5 mm to 3.5 mm, the Q factor decreased by 38%. The Q factor decreased by 46% when the width increased from 0.5 mm to 1.5 mm. The Q factor slightly increased when the thickness of the apertures layer increased. The three parameter results for the apertures layer are shown in Figure 3. Therefore, a higher Q factor CFSS can be designed when the apertures are shorter and narrower.

3.3 In-Between Substrate

The properties and thickness of the in-between substrate were considered as the parameters affecting the Q factor. A higher Q factor was found when the coupling between the conductors and apertures layers was stronger. As shown in Figure 4, a higher relative permittivity, lower loss tangent and thinner thickness of the in-between substrate produced a higher Q factor for the CFSS.

3.4 Periodicity

The periodicity of the conductors and apertures is another parameter that affects the Q factor. In Section 3.1, the Q factor increased by 13% when the conductors length was increased from 2.5 mm to 3.5 mm and by 3% when the width was increased from 0.5 mm to 1.5 mm. In Section 3.2, the Q factor decreased by 38% when the conductors length was increased from 2.5 mm to 3.5 mm and by 46% when the width was increased from 0.5 mm to 1.5 mm. It was found that the Q factor was more strongly dependent on the apertures dimensions than the conductors dimensions. The simulated results of different number of rows of conductors/apertures are shown in Figure 5. The Q factor, as expected, decreased when there were more rows of the conductors/apertures. As a result, it is preferred to have fewer rows of the conductors/apertures in the CFSS structure to achieve a higher Q factor.
3.5 Air-Gap Between Waveguide Halves

Another possible factor that could affect the Q factor was the air-gap between the waveguide halves. However, from the simulation results shown in Figure 5, the Q factor was not affected when the air-gap existed. The leaking caused by air-gap increased the insertion loss, but did not affect the resonant frequency or the Q factor.

The considered parameters and effects for Q factor are summarized in Table 1. It can be observed that to obtain the highest Q factor, the conductors should be longer; the apertures should be shorter and narrower; the in-between substrate should be thinner, be low loss and have a high relative permittivity; the periodicity should be larger with fewer rows of conductors/apertures.

Table 1: Summary of parameter effects on the Q factor

| Parameter          | Range          | Q factor effect when parameter increased |
|--------------------|----------------|-----------------------------------------|
| Conductor Length   | 1.5 to 4.5 mm  | Increase                                |
| Width              | 0.1 to 1.9 mm  | Slightly Decrease (Negligible effect)   |
| Thickness          | 0.0175 to 0.14 mm | Slightly Increase (Negligible effect)  |
| Aperture Length    | 1 to 3.5 mm    | Decrease                                |
| Width              | 0.1 to 1.9 mm  | Decrease                                |
| Thickness          | 0.0175 to 0.14 mm | Slightly Increase (Negligible effect)  |
| In-Between Substrate Relative Permittivity | 2 to 10 | Increase |
| Loss Tangent       | 0.001 to 0.019 | Decrease                                |
| Thickness (mm)     | 0.06 to 0.18   | Decrease                                |
| Periodicity Number of Rows | 1 to 4 | Decrease |
| Air-Gap (mm)       | 0.05 to 0.45   | No Effect                               |

4 CFSS Measurements

A CFSS was designed and fabricated using material Rogers XT/duroid 8100 as shown in Figure 6. The data were: conductors length \( l_c = 5 \) mm; conductors width \( w_c = 0.5 \) mm; conductors layer thickness \( t_c = 0.017 \) mm; apertures length \( l_a = 2.5 \) mm; apertures width \( w_a = 0.5 \) mm; apertures layer thickness \( t_a = 0.017 \) mm; in-between substrate: relative permittivity \( \varepsilon_r = 3.54 \); loss tangent \( \tan \delta_\varepsilon = 0.0049 \) and thickness \( d_s = 0.05 \) mm. The CFSS consisted of one row of five conductors/apertures. The simulation results were compared to the measurements using two different VNA systems and demonstrated a very good agreement as shown in Figure 7.

5 Conclusion

The effect of the physical and dielectric parameters in the CFSS structure for a higher Q factor has been studied and presented in this paper. A CFSS sample was designed and fabricated. The measurement results of the sample from two different VNA systems have also shown a very good agreement with the simulations which highlights the repeatability of the measurements. Future work will consider potential capability of the CFSS in a waveguide to be used for dielectric property measurements.

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