Magnetic field measurements of $\epsilon$ Eridani from Zeeman broadening

L. T. Lehmann, A. Künstler, T. A. Carroll, and K. G. Strassmeier

Leibniz-Institut für Astrophysik Potsdam (AIP), An der Sternwarte 16, D-14482 Potsdam, Germany

Received 2014, accepted 2015
Published online 2015

Key words stars: magnetic fields, stars: activity, stars: late-type, stars: individual ($\epsilon$ Eri), techniques: spectroscopic

We present new magnetic field measurements of the K2 main-sequence star $\epsilon$ Eri based on principal components analysis (PCA) line-profile reconstructions. The aim of this paper is to quantify the surface-averaged magnetic field and search for possible variations. A total of 338 optical echelle spectra from our robotic telescope facility STELLA with a spectral resolution of 55,000 were available for analysis. This time-series was used to search for the small line-profile variations due to a surface magnetic field with the help of a PCA. Evidence for a spatial and temporal inhomogeneous magnetic field distribution is presented. The mean, surface averaged, magnetic field strength was found to be $\langle B \rangle = 186 \pm 47$ G in good agreement with previous Zeeman-broadening measurements. Clear short-term variations of the surface averaged magnetic field of up to few tens Gauss were detected together with evidence for a three-year cycle in the surface-averaged magnetic field of $\epsilon$ Eri.

1 Introduction

$\epsilon$ Eri is among the bright stars that are mildly magnetically active and were a planet detection had been claimed. Low-amplitude radial velocities variations of $\epsilon$ Eri were first reported by Campbell et al. (1988), Hatzes et al. (2000) had announced a planet around $\epsilon$ Eri with an orbital period of 2500 d and an eccentricity of 0.6. Benedict et al. (2006) and Reffert & Quirrenbach (2011) refined the orbital solution and combined the radial velocities with astrometric observations and derived a likely mass for the planet of 1.55 $M_{\text{Jup}}$. However, Zechmeister et al. (2013) could not confirm the existence of this planet from higher-precision radial-velocity data nor did Anglada-Escudé & Butler (2012) succeed to coherently combine the different radial velocity data sets with the original 2500-d period.

Detailed studies of the basic parameters of $\epsilon$ Eri were derived from high-resolution spectroscopy by Steenbock & Holweger (1981), Drake & Smith (1993), Valenti et al. (1995), Rüedi et al. (1997), among others, and from optical interferometry by Baines & Armstrong (2012). These studies converged on the picture that $\epsilon$ Eri is a single, moderately-young ($\approx$ 800 Myr), K2 main-sequence star with an effective temperature of 5100 K, a mass of 0.82 $M_{\odot}$, a radius of 0.74 $R_{\odot}$, subsolar metallicity of $-0.17$, and barely resolvable rotational line broadening ($v \sin i = 1.6 \text{ km s}^{-1}$). The stellar rotation period was first determined from the Mt. Wilson H&K data to 11.10 d by Gray & Baliunas (1995), its range further discussed in Donahue et al. (1995). Time-series photometry was obtained by Frey et al. (1991) and from the 12 spots detected with a rotation period of between $\approx$ 10–12 d a differential rotation very much equal to the Sun’s was derived. Croll et al. (2006), Fröhlich (2007), and Savanov (2009) analyzed photometric data from the MOST satellite and found two spots or spot groups separated by 180° in longitude and individual spot rotation periods of 11.35 d and 11.55 d from which a differential surface rotation of roughly half the solar value was derived.

Gray & Baliunas (1995) found evidence of a 5-year activity cycle from Mt. Wilson H&K observations. The cycle period was revised just recently by Metcalfe et al. (2013) from a 45-yr long Ca II H&K data set based on Mt. Wilson, CTIO, Lowell, CASLEO, CPS, and HARPS observations. They found two coexisting 2.95±0.03 yr and 12.7±0.3 yr periods with evidence for a Maunder minimum-like state in the late 1980’s followed by the resurgence of a coherent 3-year cycle.

The line broadening of $\epsilon$ Eri due to a magnetic field was first announced by Marcy (1984) and Gray (1985). Marcy (1984) inferred a surface magnetic field between 620 G and 2850 G and a filling factor, $f$, between 0.89 and 0.2, respectively. These values were confined to 1 kG and $f = 0.35$ in subsequent work by Basri & Marcy (1988) and Mary & Basri (1989). Gray (1995) obtained a magnetic field strength of 1.9 kG and $f = 0.3$. Saar (1988) improved the detections by consequently applying radiative-transfer techniques in magnetized atmospheres but still obtained rather different magnetic-field values between 0 and 3.5 kG from different spectral lines. He, among others, pointed out the limitation due to substantial systematic effects in the data, in particular due to line blending. First infrared magnetic-field measurements from Zeeman broadening were presented by...
Valenti et al. (1995) and yielded a photospheric coverage of just 8.8% with a 1.44 kG field. Rüedi et al. (1997) re-discussed the impact of blending and confined the spatially averaged surface field strength on $\epsilon$ Eri to 165±30 G and concluded that it is difficult (at best) to separate $f$ and $B$. Finally, Kochukhov et al. (2011) presented modern linear and circular polarization observations with the new HARPS spectropolarimeter. The Stokes-V profiles of $\epsilon$ Eri changed systematically from night to night throughout the rotation period of the star. The mean longitudinal magnetic field varied between $-5.8 \pm 0.1$ G and $+4.7 \pm 0.1$ G. Recently, Jeffers et al. (2014) could also detect variations in the large-scale magnetic field geometry. They examined the evolution of the magnetic field topology of $\epsilon$ Eri using spectropolarimetric observations and Zeeman-Doppler imaging for six observational epochs spread over a period of nearly seven years. They found similar $S$-index variation for the last seven years as Metcalfe et al. (2013) including the hint of a three year cycle. Using Zeeman-Doppler imaging Jeffers et al. (2014) showed a highly variable magnetic field geometry. The poloidal component varies from strong dipolar to monopolar and the toroidal component varies from being non-existent to being the dominant component of the magnetic field energy.

In this paper, we present and analyze time-series optical spectroscopy of $\epsilon$ Eri. We employed our robotic telescope STELLA-II and its echelle spectrograph SES in Tenerife. Section 2 presents and describes the new data, Sect. 3 describes the Zeeman-broadening PCA technique and Sect. 4 presents the results. Our conclusions are presented in Sect. 5.

2 Observations and data reductions

Echelle spectroscopy was taken with the 1.2 m STELLA telescopes between July 2008 and October 2013. Spectra were taken with an exposure time of 300 s and achieved a signal-to-noise ($S/N$) ratio between 400:1 to 100:1 per resolution element depending on weather conditions. A total of 338 spectra were used in this analysis. STELLA-I and STELLA-II are fully robotic telescopes that make up the STELLA observatory at the IZANA ridge on Tenerife in the Canary islands (Strassmeier et al. 2004 [2010]). The fiber-fed STELLA Echelle Spectrograph (SES) is the one telescope’s only instrument. It is a white-pupil spectrograph with an R2 grating with two off-axis collimators, a prism cross disperser and a folded Schmidt camera with an E2V 2k×2k CCD as the detector (until mid 2012). All spectra have a fixed format on the CCD and cover the wavelength range from 388–882 nm with increasing inter-order gaps near the red end starting at 734 nm towards 882 nm. The resolving power is $R=55,000$ corresponding to a spectral resolution of 0.12 Å at 650 nm (3-pixel sampling). An example spectrum is shown in Fig. 1. We note that the SES received a major upgrade in summer 2012 with a new cross disperser, a new optical refractive camera, and a new 4k×4k CCD. A bit earlier, the SES fiber was moved to the prime focus of the second STELLA telescope in 2011. Further details of the performance of the system were reported by Weber et al. (2012) and Granzer et al. (2010).

Data reduction is performed automatically using the IRAF-based STELLA data-reduction pipeline (Weber et al. 2011). Images were corrected for bad pixels and cosmic-ray impacts. Bias levels were removed by subtracting the average overscan from each image followed by the subtraction of the mean of the (already overscan subtracted) master bias frame. The target spectra are flat fielded with a nightly master flat which has been normalized to unity. The nightly master flat itself is constructed from around 50 individual flats observed during dusk, dawn, and around midnight. After removal of the scattered light, the one-dimensional spectra were extracted with the standard IRAF optimal extraction routine. The blaze function was then removed from the target spectra, followed by a wavelength calibration using consecutively recorded Th-Ar spectra. Finally, the extracted spectral orders were continuum normalized by dividing them with a flux-normalized synthetic spectrum of the same spectral classification as the target in question.

3 Magnetic field measurement

3.1 PCA reconstruction of the Zeeman pattern

The principal component analysis (PCA) or Karhunen-Loeve transformation (Bishop 1995) is a multivariate algo-
algorithm, that is able to analyze tiny variations in time series. The PCA algorithm decomposes the entire data set of observed Stokes I profiles into a new coordinate system, which is of advantage to detect the directions of high variances (see Martínez Gonzalez et al. (2008) and Carroll et al. (2009)). The new basis has to explain the largest amount of variances of the data set by using as few as possible orthogonal basis vectors. The PCA computes this set of new basis vectors by calculating the eigenvectors of the covariance matrix of the data. The eigenvectors, also called eigenprofiles, are ordered by their associated eigenvalues. Therefore, the PCA will project the systematic and most coherent features to the first few eigenprofiles and will separate them from noise and from each other.

With a set of computed eigenprofiles $f_i(\lambda)$, one can reconstruct the Stokes I profiles $I(t, \lambda)$ by

$$I(t, \lambda) = \sum_i c_i(t) f_i(\lambda)$$

(1)

where $c_i(t) = I(t, \lambda) f_i(\lambda)$ is the scalar product between the Stokes I profile $I(t, \lambda)$ and the eigenprofile $f_i(\lambda)$. The coefficient $c_i(t)$ is therefore a measure for how strong a certain feature, characterized by an eigenprofile $f_i(\lambda)$, is present in the Stokes I profile given at time $t$.

It is well known that the magnetic field affects spectral lines in a certain way. An example is shown in Fig. 2. We simulate the Fe i 6173 Å line without magnetic field and with a magnetic field of 1300 G on conditions similar to ε Eri. It is clearly visible that the magnetic field leads to broadened line wings and thus decreased line depth. The variations in the activity of ε Eri will produce tiny variations with similar shape in the spectral lines. To detect such little specific variations in the time series we used the PCA. Skumanich & López Ariste (2002) demonstrated the physical content of PCA applied to Stokes profiles. They used the weak field approximation, which assumes that the magnetic field is weak enough to represent the Stokes I profiles by the low order terms of its Taylor series.

$$I(t, \lambda) = I_0(t, \lambda) + \alpha(t) \frac{\partial I_0}{\partial \lambda} + \beta(t) \frac{\partial^2 I_0}{\partial \lambda^2} + \ldots,$$

(2)

where $I_0(t, \lambda) = c_0(t) I_0(\lambda)$. Skumanich & López Ariste (2002) show that the coefficient $\alpha(t)$ could be associated with the line-of-sight velocity $v_{los}$ and $\beta(t)$ with the magnetic Zeeman splitting $\Delta \lambda_Z$. With the help of Jefferies et al. (1989) they showed that

$$\beta(t) \equiv (1 + \cos^2 \phi) \frac{\Delta \lambda_Z}{2},$$

(3)

where $\Delta \lambda_Z = \frac{e_0 B(t)}{2m_e c^2} \Delta \lambda$, so that $\beta(t) \propto B^2(t)$. Skumanich & López Ariste (2002) and Jefferies et al. (1989) emphasized that the variations caused by magnetic fields will have the shape of the second derivative of the Stokes I profiles and could be analyzed by its coefficients.

To prove this prediction, we create a set of 101 synthetic Fe i 6173 Å line profiles which vary in line-of-sight velocity from 0 – 500 m s$^{-1}$ and in the magnetic field from 0 – 300 G. In Fig. 2 the average mean profile and its first and second derivative is shown, Fig. 3 (the row below) shows the first three eigenprofiles computed by the PCA. The first and second eigenprofile matches very well with the first and second derivative, as the theory predicted. The variations in velocity and magnetic field are orthogonal to each other and can be separated by PCA. Additionally, the zeroth eigenprofile shows the shape of the average synthetic line, as expected, because the greatest variation of the Stokes I profiles to a zero-line profile is the average line profile. Therefore, the PCA algorithm enables us to detect tiny variations caused by the magnetic field in our time series of 338 Stokes I spectra.

### 3.2 Selection of spectral lines and denoising

Spectral lines are selected from the VALD-II database (Kupka et al. 1999). The selection focused on lines of approximately equal strength, as unblended as possible, and with a high Landé factor. As threshold we set 0.8 in the line depth and a minimum Landé factor of 1.59. A total of 30 such lines were selected and are listed in Table 1. For these lines we expect a comparable dependency on other line-broadening mechanisms. All 30 individual spectral lines were transformed into velocity space and averaged to obtain mean spectral lines profiles. Therefore, the S/N-ratio increased by approximately a factor of five. In Fig. 4 we show the 338 normalized spectral lines profiles we used as our Stokes I profiles for analysis.
3.3 Eigenprofiles analysis

To make the PCA more sensitive to small variations in the wings of the spectral lines profiles, we analyzed the inverted (1–Stokes I) profiles.

Fig. 3 shows the comparison of the theoretical expectations with our analysis results. The first row, Fig. 3a, shows the average profile over all spectra in the left panel, and its first and second derivative in the other panels. It illustrates the pattern we are looking for. The second row, Fig. 3b, shows the zeroth, first, and second eigenprofile of the spectral lines profiles derived with PCA. The zeroth eigenprofile in the left column represents the mean profile of the 338 spectral lines profiles. As expected, the variations of the second eigenprofile match the second derivative of the observed averaged profile. The variations are in good agreement with a correlation coefficient of 82%. This correlation indicates, following Skumanich & López Ariste (2002), variations in the magnetic field affecting the spectral lines on ε Eridani from Zeeman broadening.

The coefficients of the second eigenprofile $c_2(t)$, shown in Fig. 4, can now be used to quantify the magnetic field and its variations. A coefficient of $c_2(t) \approx 0$ represents the average magnetic field at time $t$, while positive and negative coefficients represent accordingly weaker or stronger fields. The coefficients in Fig. 4 show roughly a long-term oscillation around zero. We also see scattering of the coefficients.

Table 1 Spectral lines used in this analysis.

| El. | λ (Å) | Landé factor | El. | λ (Å) | Landé factor |
|-----|-------|--------------|-----|-------|--------------|
| Cr I | 4545.953 | 1.92 | Fe I | 4903.310 | 2.24 |
| Cr I | 4591.391 | 2.00 | Fe II | 4923.927 | 1.69 |
| Fe I | 4602.941 | 1.74 | Fe I | 4938.814 | 2.01 |
| Fe I | 4611.279 | 1.89 | Cr I | 4942.496 | 1.85 |
| Cr I | 4616.124 | 1.67 | Cr I | 4964.927 | 2.17 |
| Cr I | 4626.173 | 2.01 | Fe I | 4967.897 | 1.88 |
| Fe I | 4635.846 | 2.09 | Fe I | 5044.211 | 1.77 |
| Fe I | 4673.270 | 1.84 | Cr I | 5348.315 | 1.59 |
| Fe I | 4690.138 | 2.16 | Mn I | 5394.677 | 1.86 |
| Fe I | 4704.948 | 2.49 | Mn I | 5432.546 | 2.14 |
| Mn I | 4754.042 | 1.65 | Fe I | 5497.516 | 2.26 |
| Fe I | 4768.396 | 1.62 | Fe I | 5501.465 | 1.88 |
| Mn I | 4783.427 | 1.97 | Fe I | 5506.779 | 2.00 |
| Fe I | 4848.883 | 2.01 | Fe I | 6213.430 | 2.00 |
| Fe I | 4878.211 | 3.00 | Fe I | 6219.281 | 1.66 |

Fig. 4 The 338 normalized spectral lines profiles used for magnetic-field analysis with PCA.
Fig. 5  Comparison of theoretically expected profile patterns with results from PCA. a The observed averaged spectral lines profile and its first and second derivative. b The first three eigenprofiles of the spectral lines profiles.

on small time scales. The single seasons are clearly separated by different seasonal mean coefficients. In the next step, we will convert the coefficients to values of magnetic field.

3.4 Magnetic field determination

The actual quantification of the magnetic field, is done through a least-squares comparison of the coefficients from the observations with synthetic profiles of known \( B \cdot \sqrt{f} \). We assumed \( f = 1 \) to obtain a surface average magnetic field and generated 1,000 synthetic profiles with \( B \cdot \sqrt{f} \) between 0 G and 333 G to analyze this series with PCA. The resulting \( c_2(t) \) coefficients relate linearly with \(( B \cdot \sqrt{f})^2\), see Eq. (3), and a simple regression then defines the transformation to surface-averaged magnetic field strength. With the help of the calibration curve, Fig. 7 we convert the coefficients of the second eigenprofile \( c_2(t) \) to magnetic field values \( B \cdot \sqrt{f} \). Hereinafter we defined for the surface average magnetic field

\[
B \cdot \sqrt{f} = \langle B \rangle.
\]
4 Results

4.1 The magnetic field of \( \epsilon \) Eri

Fig. 8 shows all 338 individual \( \langle B \rangle \) measures with its uncertainties. We measure a mean magnetic field over all seasons of \( 186 \pm 47 \) G, where the error represents the standard deviation. The mean magnetic fields of single seasons are listed in Table 2. We see that the average magnetic field of the single seasons is oscillating with maxima in the seasons 2009/2010 and 2012/2013 and minima in 2011/2012 and 2013/2014. The variations in single seasons are largest in the seasons 2011/2012 and 2012/2013 and smallest in the season 2013/2014. In the very end of season 2009/2010, we clearly see a separated group of few observations where magnetic field values are higher as in the rest of the season. Season 2010/2011 consists of only 10 observations, which makes the variation analysis not reliable, but the data points fit in the overall trend.

Another issue from Fig. 8 is that the magnetic field values vary over few tens of Gauss at significantly shorter time scales than the rotation period of \( \epsilon \) Eri. Their average internal errors are \( \pm 13 \) G. Short-term variations on a \( 1-5 \sigma \) level are evident within an observing season. This could be an indication that the topology of \( \epsilon \) Eri’s magnetic field is spatially inhomogeneous. The strong variations could appear from local active regions which rotate in and out of the line of sight. This would be in a good agreement to the large-scale magnetic field geometry determined by Jeffers et al. (2014). A periodogram analysis does not reveal a significant short period, which could be interpreted as an indicator for temporal inhomogeneities of the active regions.

Temperature surface inhomogeneities like starspots may contribute to the disk-integrated line strength, and thus its broadening, even if the spots remain unresolved. Because in the present paper it is our intention (like in most other Zeeman-broadening works) to determine the surface averaged magnetic field, one of the built-in limitations is the still common (but surely simplified) homogeneous two-component photospheric model, i.e. two magnetic components described by a single temperature model (see also Sect. 6.4 in Valenti et al. (1995) for a detailed discussion of the possible error budget of this assumption).
4.2 Time variability

Fig. 8 shows a sine-curve fit to the magnetic-field data that indicate a period of 3.0 yr (solid line). In Fig. 9 the corresponding periodogram is given.

Hatzes et al. (2000) were the first to report a 3-years magnetic activity cycle in \( \epsilon \)-Eri. Recently Metcalfe et al. (2013) suggested the simultaneous existence of two cycle periods of 2.95±0.03 years and 12.7±0.3 years. They used the \( \epsilon \)-Eri H&K S-index to estimate the magnetic activity cycles. Our time series of \( \langle B \rangle \) measurements of \( \epsilon \)-Eri show a similar behavior as the published data of the \( \epsilon \)-Eri H&K S-index in Figure 1 by Metcalfe et al. (2013) and the published data of the S-index in Figure 2 by Jeffers et al. (2014).

We analyzed our time series for long-term periods with the help of a Lomb-Scargle (Scargle 1982) analysis and determine a period of 1096±471 d (3.0±1.3 yr). To estimate its false alarm probability (FAP) we used two different methods. In the first one we apply the formula of Horne & Baliunas (1986) which resulted in a FAP well below 10\(^{-7}\) for the most significant peak. For a second method, we used a bootstrap resampling technique where we randomly redistributed the eigenvalue coefficients but retained the same times for the observations (e.g., Kürster et al. 1997). A 100,000 resampling trials were performed but none had reached a power as high as our most significant peak and we estimate the FAP to be lower than 10\(^{-5}\).

The sine-curve periodicity in Fig. 8 is comparable to the trend of the \( \epsilon \)-Eri H&K S-index in Figure 1 of Metcalfe et al. (2013). We see in our data and in the S-index measurements that the activity of \( \epsilon \)-Eri is higher in 2009/2010 and lower in 2008/2009 and 2011/2012. The rise of activity in the year 2012/2013 is suggestively visible by Metcalfe et al. (2013). Also the higher variances in the years 2011/2012 and 2012/2013 are visible in the \( \epsilon \)-Eri H&K measurements as well. Good agreement is also seen for the high activity at the end of the season 2009/2010. The overall trend of our results also fits with the S-index measurements from Jeffers et al. (2014) shown in their Figure 2. The behavior of the data from 2009/2010 to 2012/2013 is similar to our results of the \( \langle B \rangle \) measurements. The last season (2013/2014) seems to be less active than the seasons before. The trend of decreasing activity in 2013/2014 is also in agreement with the S-index measurements of Jeffers et al. (2014).

5 Conclusions

Using PCA on a time series of 338 spectra, we were able to quantify the magnetic activity variations on \( \epsilon \)-Eri. We computed an average surface-mean magnetic field of 186±47 G. The analysis showed variations of the mean surface magnetic field on shorter time scales as the rotation period, which could be interpreted as spatial inhomogeneities in the magnetic field. The lack of a long-term persistent pattern on time scales of the rotation period suggests additional temporal inhomogeneities in the magnetic activity of \( \epsilon \)-Eri.

We confirm the qualitative agreement with the \( \epsilon \)-Eri H&K S-index analysis done by Metcalfe et al. (2013) and Jeffers et al. (2014). The trend of the \( \epsilon \)-Eri H&K measurements are comparable to our \( \langle B \rangle \) measurements. Our analysis shows a time variation of the magnetic field that is comparable to the shorter magnetic activity cycle estimate by Metcalfe et al. (2013). We suggest a period of 3.0±1.3 yr comparable to the 2.95±0.03 years determined by Metcalfe et al. (2013). By using longer time series spectra of \( \epsilon \)-Eri the method would principally be able to capture the longer period as well, if existent.

The analysis of time series by using PCA is a very successful tool to detect variations on cool, slowly rotating stars. The velocity variations can be separated from the magnetic field variations for a detailed analysis of time variations of the surface mean magnetic field. The method promises to be successful on further stars and will be used for analyzing variations of the average surface magnetic field on suitable targets in combination with the recently presented orthogonal matching-pursuit technique for single spectra by Carroll & Strassmeier (2014).

Acknowledgements. The STELLA project was funded by the Science and Culture Ministry of the German State of Brandenburg (MWFK) and the German Federal Ministry for Education and Research (BMBF). Its a pleasure to thank Michi Weber and Thomas Granzer for their efforts to keep STELLA running and an anonymous referee for many helpful suggestions.

References

Anglada-Escudé, G., & Butler, R. P. 2012, ApJS, 200, 15
Baines, E. K., & Armstrong, J. T. 2012, ApJ, 748, 72
Basri, G., & Marcy, G. W. 1988, ApJ, 330, 274
Benedict, G. F., McArthur, B. E., Gatewood, G., et al. 2006, AJ, 132, 2206
