Mid Infrared Optical Gas Sensor Using Plasmonic Mach-Zehnder Interferometer

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In this work, we propose an optimized design for on-chip gas sensor using metal-insulator (MI) plasmonic waveguide in the mid infrared range and utilizing a Mach-Zehnder Interferometer (MZI). The MI waveguide utilizes a high index dielectric layer on top of the metal to enhance the sensitivity of the sensor. The thickness and the refractive index of this layer are optimized to achieve high sensitivity. Using this layer, a design that exhibits high performance for both wavelength and intensity interrogation schemes is achieved. In addition, another one that furtherly enhances the sensor performance for intensity interrogation is also proposed. This design also minimizes the sensor sensitivity to wavelength variations. Intensity interrogation scheme has the advantage of eliminating the size and cost needed by wide wavelength band measurements including either spectrometer or tunable laser in wavelength interrogation. The first design sensitivity has reached 10000 nm/RIU with wavelength interrogation figure of merit (FOM\(_\lambda\)) of 133RIU\(^{-1}\) and intensity interrogation FOM, of 239RIU\(^{-1}\). While the second one exhibit FOM, of 363RIU\(^{-1}\), both with length of 250 µm around 4.6 µm wavelength. Finally, these structures are cheap, compact, and easy to fabricate.

Mid infrared region is recently attracting a great attention as due to the wide range applications. These applications include; thermal imaging, infrared spectroscopy, chemical and biological sensing\(^1-3\). The importance of this spectral region arises from the fact that many chemical and biological molecules have their characteristic absorption within this region\(^4\). Optical detection of molecules is based on intensity or wavelength change due to change in the real or imaginary part of the analyte refractive index. Both imaginary and real parts of the refractive index, of the molecules under detection, exhibit a peak around its characteristic absorption wavelength. Hence, amplifying the effect that is detected by the optical device. This fact makes mid-infrared a suitable range for biomolecular and gas detection with high sensitivity. Gases like methane CH\(_4\), carbon dioxide CO\(_2\), and carbon monoxide CO have high absorption around 3.2 µm, 4.3 µm and 4.6 µm wavelengths, respectively.

Many refractive index gas sensors – refractometers – were proposed recently\(^5-8\), where the real part (n) of the refractive index is detected. Refractive index sensors have the advantage of ultra-small sample volume as its sensitivity does not depend on the sample volume, and hence are promising for integrated on chip sensors\(^9\). Most of the proposed refractive index gas sensors are working in the near infrared, and hence do not benefit from the signal amplification that happens to the gas refractive index in the MIR.

In general, there are two main sensing schemes for the refractive index sensors; the wavelength interrogation, and the intensity interrogation\(^10\). The wavelength interrogation scheme is based on the resonant wavelength shift with the change in the analyte refractive index. On the other hand, the intensity interrogation scheme is based on the intensity shift at a certain detection wavelength. Detecting the real part of the refractive index using wavelength interrogation requires either a spectrometer or a tunable laser, which will add to the size and cost of the sensor. However, many of the previously proposed refractive index gas sensors utilized wavelength interrogation\(^5-8\).

Surface plasmon resonance SPR sensors have achieved very high sensitivity, up to 13800 nm/RIU\(^11\), using the well-known method of attenuated total reflection (ATR) proposed by Kretschmann\(^12,13\). However, the large sizes of the SPR sensors prohibit them from being integrated on a single chip, as usually required for producing portable low-cost sensors. Moreover, the SPR sensors require careful alignment, thus, they lack strongly needed advantages such as rapid and high throughput measurements. Many efforts have been done to overcome these

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drawbacks, using nanoplasmonic structures like nanoparticles, nanoslit arrays and nanohole arrays\textsuperscript{14–16} to obtain low cost, small size and high throughput sensors. However, these efforts are lacking the high sensitivity that can be achieved using the conventional SPR sensor, with best sensitivity of 560 nm/RIU obtained by the nanoslits.

Mach-Zehnder Interferometer (MZI) is one of the well-known label free optical sensing devices, which can achieve high sensitivity\textsuperscript{17–19}. Plasmonic waveguides with different configurations such as Metal-Insulator (MI)\textsuperscript{12}, Insulator-Metal-Insulator IMI\textsuperscript{20,21} and Metal-Insulator-Metal (MIM)\textsuperscript{22–25}, as well as plasmonic directional couplers\textsuperscript{26} can be used to form plasmonic MZI. Plasmonic MZI sensors were recently proposed for ultrasensitive on chip biosensing, with sensitivity reaching 3695 nm/RIU at 730 nm wavelength, and device length of 57.6 µm\textsuperscript{27–29}. Beside the high sensitivity, this design forms on-chip easy-to-fabricate sensor. This sensor is capable for rapid, portable and high throughput operation using multiplexed array sensing. Finally, it can be integrated with microfluidic channel on the same chip.

Many difficulties are faced when trying to design plasmonic gas sensors in the MIR range. Plasmonic waveguide sensitivity is proportional to refractive index to be sensed, and inversely proportional to the operating wavelength. In this paper a MIR gas sensor is proposed using the vertical MZI structure in\textsuperscript{29}. High sensitivity up to 10000 nm/RIU and high figure of merit (FOM) are achieved. To achieve this performance, a high index layer is used above the metal of the sensing arm. The sensor analysis and design are done using finite difference time domain (FDTD) solver\textsuperscript{30}. Two sensor designs are proposed; the first design is optimized for wavelength interrogation like many of the previously published refractive index sensors\textsuperscript{5–8,27–29,26}, while the second design is optimized for intensity interrogation scheme, which possesses the advantages of high compactness and low cost. These designs have all the advantages of the previously proposed liquid MZI sensor\textsuperscript{26}, in addition to, its high sensitivity to gaseous medium and operation in the mid infrared, around the characteristic absorption of gases.

In section II, the plasmonic MZI sensor structure is presented together with the sensor performance parameters and the design approach. Section III proposes the metal-insulator (MI) waveguide with high index layer to enhance the performance of the plasmonic MZI sensor. Section IV is devoted for the implementation of the gas sensor designs, and the finite difference time domain (FDTD) simulation results and optimization. Finally, the conclusion is given in section V.

**Results and Discussions**

**Structure and MZI analysis.** The proposed structure consists of three layers: metal-sapphire-metal above a sapphire substrate, which forms MIM and MI waveguides that construct the MZI reference and sensing arms, respectively, see Fig. 1. The sapphire is chosen due to its low absorption in the wavelength range 1.1–6 µm\textsuperscript{31}, and the metal used is silver (Ag). The input plane wave, from the substrate, is coupled to the MIM and MI waveguide modes through the input slot of width \(w_1\), then each mode propagates with its propagation constant (\(\beta\)) distance \(L\), and finally coupled out through the output slot \(w_2\) and interfere with each other.

The output signal intensity is given by:

\[
\frac{I_{\text{out}}}{I_{\text{in}}} = (A + B)^2 - 4AB \sin^2 \left( \frac{2\pi(n_{\text{eff, MI}} - n_{\text{eff, MIM}})L}{\lambda} \right) \]  

(1-a)

With resonant wavelength \(\lambda_{\text{res}}\) and FSR, equal to:

\[
\lambda_{\text{res}} = \frac{(\Delta n_{\text{eff}} \times L)}{q} \]  

(1-b)

\[
\text{FSR}_\lambda = \frac{\lambda^2}{(\Delta n_{\text{eff}} \times L)} \]  

(1-c)

and

\[
\Delta n_{\text{eff}} = n_{\text{eff, MI}} - n_{\text{eff, MIM}} \]  

(1-d)
where q is an integer number, \( \Delta n_{\text{eff}} \) is the difference between the MI and MIM effective indices, \( A = a_1 a_2 \exp(-\gamma_1 L) \) and \( B = b_1 b_2 \exp(-\gamma_2 L) \) are the normalized output power of MIM and MI mode respectively, with \( a_1, a_2 \) and \( b_1, b_2 \) and \( \gamma_1, \gamma_2 \) are the input, output coupling coefficients and losses of MIM and MI modes, respectively.

One can easily derive the MZI sensitivity \( \frac{d\lambda}{dn} \) and the full width half maximum (FWHM) from (1) and get:

\[
S = \frac{d\lambda}{dn} = \frac{\lambda}{\Delta n_{\text{eff}}} \frac{d_{\text{eff MI}}}{dn} = \frac{\lambda}{\Delta n_{\text{eff}}} S_{\text{wg}}
\]

(2)

where \( S_{\text{wg}} = \frac{dn_{\text{eff MI}}}{dn} \) is the MI waveguide sensitivity.

\[
\text{FWHM}_\lambda = \frac{\lambda^2}{\pi L (n_{\text{eff MI}} - n_{\text{eff MIM}})} \frac{\sqrt{2AB}}{\pi} \frac{\text{FSR}_\lambda}{A + B}
\]

(3)

It can be deduced from (2) that the MZI sensitivity increases linearly by increasing the wavelength; however, the FWHM increase with wavelength is quadratic. In the wavelength interrogation method, the minimum detected refractive index change \( \Delta n \) is determined by the FWHM. While, in intensity interrogation method, the sensor performance is determined mainly by intensity changes. Thus, for better performance sensor, a figure of merit FOM is defined. For wavelength interrogation scheme, the FOM is defined as:

\[
\text{FOM}_\lambda = \frac{d\lambda}{dn} \frac{S_{\text{wg}}}{\text{FWHM}_\lambda}
\]

(4)

And for intensity interrogation scheme, the FOM is defined as:

\[
\text{FOM}_I = \frac{1}{I} \frac{dI}{dn}
\]

(5-a)

From (1) we get:

\[
\frac{dI}{dn} \propto 2 \sin \left( \frac{\Delta \varphi}{2} \right) \cos \left( \frac{\Delta \varphi}{2} \right) \frac{d\Delta \varphi}{dn} = \sin (\Delta \varphi) \frac{\pi L \lambda}{S_{\text{wg}}}
\]

(5-b)

For \( A = B \) we will get:

\[
\text{FOM}_I \propto \sin (\Delta \varphi) \frac{d\lambda/dn}{\text{FWHM}_\lambda} = \sin (\Delta \varphi) \text{FOM}_\lambda
\]

(5-c)

Equation (5-c) shows that optimizing FOMI is also optimizing FOM\(_\lambda\). Hence, to achieve high detection performance we have to: increase the MI waveguide sensitivity \( S_{\text{wg}} \), decrease waveguides losses, equalize both modes output power \( (A = B) \), for minimum FWHM, increase MZI length, and work at low wavelengths. To suppress the effect of different wavelength regions when comparing with other designs, we will also compare the term \( L/\lambda \).

So, in our design, we are trying to increase the sensitivity of the MI waveguide, decrease waveguides losses and balance the modes output power.

**Reference arm: Metal-Insulator-Metal waveguide performance.** In principle, MIM waveguide support two TM modes one with symmetric and another one with antisymmetric transversal electric field component \( (E_x) \). However, the symmetric mode is of more interest as the antisymmetric mode suffers from low confinement and exhibit cut-off at small slot widths. As mentioned previously, MIM waveguide is the reference arm of our MZI sensor, with silver and sapphire as the metal and insulator, respectively. The symmetric mode profile of our MIM waveguide with \( D = 600 \text{ nm} \) is shown in Fig. 2a. Our MIM waveguide exhibit higher effective...
index compared to the MI sensing arm (which is almost one for gaseous medium) due to the high field confinement within the slot\(^2\)\(^4\)\(^5\), see Fig. 2b. MIM mode effective index increases as the slot width and wavelength decrease, Fig. 2b. In general, operating at wavelengths closer to the metal plasma wavelength increase the confinement and hence the effective index of the plasmonic waveguides\(^1\)\(^2\)\(^3\); the silver used here has plasma wavelength around 280 nm\(^3\)\(^2\). However, as effective index increases as the MIM mode intrinsic losses increase significantly compared to MI mode losses (which is around 0.001 dB/\(\mu\)m for gaseous medium), see Fig. 2c.

Sensing arm: Metal-Insulator waveguide performance. The design of high performance plasmonic MZI gas sensor in the MIR region using MI waveguide as the sensing arm has two main challenges: 1) The MI waveguide sensitivity (\(S_{\text{wg}}\)) is small for two reasons. Firstly, the sensitivity decreases as the insulator index decreases. So, for gas sensing, the sensitivity of the MI waveguide is lower than that of the higher index biomolecules; liquid sensing. Another reason is that the sensitivity of the waveguide decreases as the operating wavelength gets far from the metal plasma resonance wavelength. 2) MI waveguide with low-index gas as the insulator material results in MI waveguide losses much lower than that of the MIM waveguide, see Fig. 2c, which according to (3) increases the FWHM (as \(A \ll B\), while minimum at \(A = B\)). Hence, according to (4) this will result in low FOM as the two main parameters \(S_{\text{wg}}\) and FWHM are deteriorated.

To overcome all these issues at once, a high index layer (HIL) is introduced above the metal of the MI waveguide, as shown in Fig. 3a, forming MII waveguide\(^3\)\(^3\)\(^3\)\(^3\). Using Maxwell equations, we can obtain the dispersion relation of the TM mode in a metal-insulator-insulator (MII) waveguide, Fig. 3b,c, as follows\(^3\)\(^6\):

\[ k_{id} \approx \frac{\tan^{-1}(f) + \tan^{-1}(g)}{\mu_2} \quad (6-a) \]

with

\[ f = \frac{\varepsilon_2 \mu_1}{\varepsilon_1 \mu_2} \quad (6-b) \]

and

\[ g = \frac{\varepsilon_3 \mu_3}{\varepsilon_3 \mu_2} \quad (6-c) \]

Figure 3. (a) Vertical plasmonic MZI with high index layer (HIL), (b) MII waveguide mode major component \(E_x\) with silver and HIL with index 2.4 and thickness 320 nm at \(\lambda = 4.5\ \mu\)m with metal/HIL interface at \(x = 4.7\ \mu\)m, (c) MII waveguide.

Figure 4. Sensitivity and Losses of the MI waveguide versus: (a) HIL refractive index with \(h_{\text{HIL}} = 250\ \text{nm}\) at \(\lambda = 4.\ \mu\)m and (b) \(\text{Si}_3\text{N}_4\) thickness (\(h_{\text{HIL}}\)) at \(\lambda = 4.5\ \mu\)m.
and

$$u_1 = \sqrt{\varepsilon_1 - \varepsilon_2}, \quad u_2 = \sqrt{\varepsilon_2 - \varepsilon_3}, \quad u_3 = \sqrt{\varepsilon_3 - \varepsilon_1}$$

(6-d)

where $d$ is the HIL thickness, $\varepsilon_1 = \varepsilon_m$ is the metal permittivity, $\varepsilon_3 \approx 1$ the sensing medium permittivity and $\varepsilon_2 > \varepsilon_3$ is the high index layer permittivity, $n_{\text{eff}}$ the waveguide effective index, $k_0$ the free space wavenumber.
Using the previous analytical expression, we calculate the MII waveguide sensitivity for different HIL thicknesses and refractive indices. The analysis shows that this layer should be optimized regarding its thickness and index at the operating wavelength, because for large thickness and/or index of the layer, the MI mode field is confined mostly inside this layer, and hence the sensitivity decreases due to the weak field in the sensing medium. So, there is an optimum thickness and index for this layer to enhance the sensor performance. Therefore, we firstly perform modal analysis using finite difference solver to optimize the thickness and index of this layer for maximum sensitivity. Initial optimization shows that for 250 nm thickness of this HIL, the highest sensitivity is achieved at index of 3 for $\lambda = 4 \mu m$, as depicted in Fig. 4a. We, therefore, use silicon nitride Si$_3$N$_4$ for this layer with refractive index of 2.4 around 4.5 $\mu$m wavelength. When optimizing for the highest sensitivity at 4.5 $\mu$m wavelength, near the absorption peak of CO and CO$_2$, the thickness of Si$_3$N$_4$ is 320 nm, Fig. 4b.

The analysis shows that this HIL will solve the two main challenges mentioned previously. This layer will: 1) increase the effective index and more importantly the sensitivity ($S_{wg}$) of the MI waveguide, as shown in Fig. 5a,b, respectively. 2) increase the losses of the MI waveguide and makes it comparable to that of the MIM ($A \approx B$), see Fig. 5c, such that the FWHM according to (3) is minimized. Consequently, this will enhance the FOM significantly according to (4). Note that wavelength with higher sensitivity suffers also from higher losses. Hence, the optimum wavelength of operation, with highest FOM not sensitivity, is achieved through FDTD optimization.

**Wavelength interrogation design.** From Fig. 4b, we get that for maximum sensitivity, the thickness of the Si$_3$N$_4$ must be $h = 320$ nm at $\lambda = 4.5 \mu m$, see Fig. 4b. Now we want to design the MZI using this MII waveguide. For $\lambda = 4.5 \mu m$, we choose $D = 700$ nm, $w_1 = 2400$ nm and $w_2 = 1000$ nm in order to have efficient coupling and also equal power in both modes. For the two waveguides modes to be uncoupled, the thickness of the metal $T$ has to be greater than 1400 nm at $\lambda = 4.5 \mu m$. We initially choose $T = 1800$ nm and the MZI length to be $L = 100$ $\mu$m.

Figure 6a shows the FDTD results of the designed MZI. The sensor performance is degraded, exhibits large FWHM, around the wavelength of maximum sensitivity, $\lambda = 4.5 \mu m$. This is due to the phase difference, $\Delta \varphi = (2\pi/\lambda)^*\Delta n_{ef}*L$, of the MZI waveguides. This phase difference saturates and exhibits a maximum around 4.5 $\mu m$ wavelength, as shown in Fig. 6b. Also, the maximum transmission does not occur due to $\Delta \varphi_{res} = 2q\pi$, i.e. the resonant wavelength condition, where $q$ is integer. However, it always happens at the wavelength of maximum $\Delta \varphi$. Thus, resulting in almost zero wavelength shift ($d\lambda/dn \approx 0$) and accordingly very low FOM$_{\lambda}$ (4).

**Figure 8.** Vertical plasmonic MZI with $D = 900$ nm, $T = 1500$ nm, $h_{HIL} = 240$ nm, $w_1 = 1550$ nm, $w_2 = 1600$ nm, $P_{gr} = 1216.2$ nm and $h_{gr} = 475$ nm. (a) Figure of Merit (FOM$_{\lambda}$) versus MZI length around $\lambda = 4.6 \mu m$. (b) Normalized output transmission versus wavelength at different medium refractive indices at $L = 250$ $\mu$m. (c) Resonance wavelength shift and output intensity fraction versus air medium refractive index change with MZI length of 250 $\mu$m around $\lambda = 4.6 \mu m$. 
We can change this response, along the wavelength, by changing waveguides dimensions. Further increase in the MIM waveguide thickness \(D\) does not result in shifting this behavior to wavelengths far from the maximum sensitivity wavelength. However, decreasing \(D\) to 100 nm or lower results in shifting \(\Delta \phi\) maximum wavelength to lower values, but this very small thickness \(D\) increases the MIM waveguide loss significantly as well, around \(0.5 \text{ dB/}\mu\text{m}\) for \(D = 100 \text{ nm}\), resulting in very weak resonance. To solve this issue, we can work on higher operating wavelength, or change the HIL thickness \((h_{\text{HIL}})\) and sacrifice the maximum sensitivity, see Figs. 4b, 5b. However, changing the HIL layer thickness to lower values is better as it results in decreasing the MI waveguide loss. Moreover, the output transmission is low and need to be increased. Thus, we used a grating on the substrate-metal interface, as shown in Fig. 7a to increase the input power coupling and hence the output power. The optimized grating dimensions are \(P_{\text{gr}} = 1216.2 \text{ nm}\), the grating period and \(h_{\text{gr}} = 475 \text{ nm}\), the grating thickness, see Fig. 7b. We then re-optimized the input and output slots, and get \(w_1 = 1550 \text{ nm}\) and \(w_2 = 1600 \text{ nm}\). This enhanced the output power of the initial design, Fig. 6a, by a factor of 3.6. Then, further optimization is done using FDTD simulations to maximize the FOM and select the suitable operating wavelength. Note that, for the MIM to support single mode, the insulator layer thickness \((D)\) must be lower than 1400 nm at 4.5 \(\mu\text{m}\) wavelength.

After FDTD optimization, the design with \(D = 900 \text{ nm}, T = 1500 \text{ nm}, h_{\text{HIL}} = 240 \text{ nm}\) at \(L = 100 \mu\text{m}\) reaches FOM of 48.4RIU\(^{-1}\), around 4.6\(\mu\text{m}\) wavelength. The length of the MZI is fixed at 100 \(\mu\text{m}\), which is only 22 times the operating wavelength. FOM increases as the MZI length increases (4) and (5). As mentioned previously, when comparing between different MZI designs, it is important to compare designs with the same \(L/\lambda\) ratio. The previously published results for similar MZI[34], working as a liquid sensor, was FOM\(_{\lambda}\) of 122RIU\(^{-1}\) and 150RIU\(^{-1}\) with \(L/\lambda\) ratio of 50 and 63.2, respectively, and wavelength around 700 nm. Figure 8a shows the FOM\(_{\lambda}\) versus MZI length for our design, with maximum length of 250 nm which corresponds to \(L/\lambda = 54\). At \(L = 250 \mu\text{m}\), Fig. 8b, our sensor reaches FOM\(_{\lambda}\) of 133RIU\(^{-1}\), around 4.6\(\mu\text{m}\) wavelength, with \(S = 10000 \text{ nm/RIU}\), FWHM \(= 75 \text{ nm}\) and FOM\(_{I}\) of 239 RIU\(^{-1}\) for refractive index change \(\Delta n = 1e-3\). Figure 8c shows the resonance wavelength shift and the output intensity change at different air medium refractive index change, with MZI length of 250 \(\mu\text{m}\).

**Intensity interrogation design.** Further investigation shows that the region where the \(\Delta \phi\) saturates and exhibits a maximum, see Fig. 6, can result in high FOM\(_{I}\) by selecting the appropriate MZI length. Although the FWHM is large and the wavelength shift \(\Delta \lambda\) is almost zero, which result in very bad FOM\(_{\lambda}\). This is because FOM\(_{I}\) depends only on the waveguide sensitivity \((S_{wg})\) of the sensing arm and the MZI length (5-b). As mentioned above, the maximum transmission always happens at the wavelength of maximum \(\Delta \phi\). Hence, the intensity change will not happen due to wavelength shift in the resonant condition, but due to the value of the \(\Delta \phi\) at the

**Figure 9.** Vertical plasmonic MZI with \(D = 1000 \text{ nm}, T = 2000 \text{ nm}, h_{\text{HIL}} = 320 \text{ nm}, w_1 = 2100 \text{ nm}, w_2 = 1800 \text{ nm}, P_{\text{gr}} = 918.4 \text{ nm}\) and \(h_{\text{gr}} = 450 \text{ nm}\). (a) Transmission spectrum at different medium indices at \(L = 250 \mu\text{m}\). (b) Output Intensity Fraction around \(\lambda = 4.6 \mu\text{m}\) versus air medium refractive index change \((\Delta n_{\text{med}})\) at \(L = 250 \mu\text{m}\). (c) Intensity interrogation FOM\(_{I}\) versus MZI length around \(\lambda = 4.6 \mu\text{m}\).
same wavelength. Also, working at this wavelength where the FWHM is increased, has another advantage; at this wavelength region the intensity change is less dependent on the output wavelength of the source. Hence, optimization is done using FDTD simulations for the MI waveguide that exhibit maximum waveguide sensitivity around 4.5 μm with hHIL = 320 nm. The optimized design dimensions are: D = 1000 nm, T = 2000 nm, hHIL = 320 nm, w1 = 2100 nm and w2 = 1800 nm. Again grating with P_g = 918.4 nm and h_g = 450 nm is used to enhance the output power around 4 times.

Figure 9a shows the transmission spectrum at different medium indices, while Fig. 9b shows the output intensity change around λ = 4.6 μm versus the surrounding medium refractive index change, both at L = 250 μm. The FOM, for different MZI lengths around λ = 4.6 μm is shown in Fig. 9c. This design shows much higher FOM, than the previous design, in Fig. 8, 363 compared to 239 at L = 250 μm.

Note that, the fabrication of such structures is not challenging. Although the silver layer is thick around 2 μm the slots are also wide, minimum of 1.5 μm, hence the fabrication is simple as the aspect ratio is still small (almost one). The work in48 and49 shows that they easily patterned a 20 μm and 40 μm thick silver layers with even much higher aspect ratio (up to 5:1). In addition there are different etchant mentioned in40 which some of them are selective to silver, other selective to sapphire and other selective to silicon nitride. It is also important to note that, the effect of the fabrication tolerances is lower in our case since the dimensions and operating wavelength are large41.

Conclusion
A free space coupled plasmonic MZI gas sensor operational in the MIR spectral region is designed and optimized. Using SiO2N4 layer in the metal-insulator arm increases the sensitivity of the sensor to 10000 nm/RIU. Two different designs have been developed and proposed. The first design is optimized for maximum wavelength interrogation, FOM = 133RIU−1, which also exhibits high intensity interrogation, FOM = 239RIU−1. While, the second design is optimized for maximum intensity interrogation, FOM = 363RIU−1, with low sensitivity to wavelength variations, both with L = 250 μm at λ = 4.6 μm. Intensity interrogation scheme have the advantage of low cost and compact size sensors. Using our sensor near the absorption fingerprints of the gases to be detected results in high performance sensors with low detection limits. Finally, the proposed sensors allow for mass-scale fabrication hence, low cost devices that are capable for real-time and high throughput sensing using multiplexed sensor arrays.

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Author contributions
M.S. has proposed structures and defined the functionality and applications. R.S. has performed the theoretical modeling and numerical simulations. M.S. has suggested and supervised the project. R.S. wrote the first draft of the manuscript. M.S. and D.K. has revised and modified the manuscript. All authors discussed, revised, edited, and approved the manuscript.

Competing interests
The authors declare no competing interests.

Additional information
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