Abstract—Classical synchronous generators have been used for decades in the field of power generation. The traditional manner of operation of these systems is the balanced, three-phase configuration. However, recently there has been an interest in re-configuring consolidated, commercial, three phase generators to operate in single phase operation. A main driver for this phenomenon is the aim of manufacturers to extend their range of products for minimum development cost. Such an approach however brings a number of design challenges, especially in terms of the elevated damper cage currents and the negative sequence currents, when a 3-phase machine is ‘forced’ to operate in 1-phase. This paper therefore investigates and analyses these challenges. Considering a commercial, 3-phase, 400 kVA alternator. Detailed models, validated against experimental validation in 3-phase operation are first obtained. The machine is then re-configured to single phase operation. This paper proposes and shows how a suitable single phase loading can be found for 3-phase generators operating in single phase.

Index Terms— Synchronous Generators, Single-Phase operation, Finite Element Analysis.

I. INTRODUCTION

The classical, wound-field, synchronous machine is the traditional candidate for power generation applications. Considering its long history, today these machines can offer high power quality, efficiency [1] and excellent overall performance [2]. Apart from being the most common power generation source in power grids [3], the wound-field synchronous generator (SG) is also used in several marine [4], automotive and aerospace environments[5]. While these classical machines are mostly known for steady state operation with balanced loads, however there is also a growing interest in terms of their operation as single-phase (1φ) generators [6]. This is especially true in the large market for 1φ operation in isolated areas where national grids are difficult to install and maintain [2]. These solutions offer a higher power-per-phase ratio compared to three-phase 3φ SGs [7] and are therefore ideal for such applications. To meet this demand for 1φ SGs, while reducing the development costs, various SG manufacturers have recently begun to investigate the migration of their 3φ products to 1φ operation. This migration strategy is done by simply re-configuring a 3φ product’s winding arrangement into a 1φ configuration, such as shown in Fig. 1.

It is very clear that if an existing 3φ product is available, then very little effort is required to achieve the 1φ version. However it does come with some technical challenges, including

1) Power rating and power density
   Theoretically, the power of a 3φ SGs working in 1φ operation is significantly less than its original 3φ rating. This implies that the power density of these machines is significantly poor.

2) The presence of negative sequence components
   The 1φ winding configuration represents effectively an unbalanced operating condition when current flows inside it. Hence, the effects of the armature reaction and the generator’s unbalanced fields result in significant negative sequence components in the machine.

3) Elevated currents in the damper cage windings
   Most classical SGs employ a damper cage winding on the rotor, which in 3φ operation has a relatively small impact on the main performance of the machine [8]. Once the machine is in 1φ operation, then the unbalanced loading condition in conjunction with the negative sequence field components could result in very high values of currents in the damper bars.

4) Efficiency
   Due to the potentially elevated current values flowing in the damper cage during 1φ operation, the ensuing losses can be significant leading to an overall efficiency deterioration which often obligates to de-rate the SG to avoid damaging due to high temperatures [9].

The main aim of this paper is to address the challenge highlighted in Point 1 above, while giving consideration to the ensuing issues related to Points 2), 3) and 4). In other words, it is proposed and investigated a methodology aimed at enhancing the performance in terms of power rating (and therefore power density) of a 3φ SG operating in a 1φ configuration. This methodology is based on the idea that the machine power rating for a 3φ SG operating in a 1φ configuration is mainly limited by the unbalanced currents in the damper cage winding and the ensuing thermal effects. Therefore, if the 1φ operation was set to be constrained by the maximum allowable damper cage currents, then theoretically the power rating of the machine in 1φ operation can be extended beyond the theoretical small portion of the original 3φ rating. The proposed hypothesis is that the maximum 1φ loading can be achieved when the total damper cage loss 1φ operation is equal to the total damper cage loss in rated, 3φ operation. This paper will therefore investigate and validate this hypothesis. As a case study, this paper considers an off-the-shelf, 400 kVA SG platform. A finite element (FE) model of the machine working in 3φ operation is first built and validated against experimental results of the SG case
study. The same model is then modified to a 1φ version and thus the 1φ loading that results in the same damper cage loss as for the rated 3φ operation can be found. The operational characteristics of the machine at this load point are then mapped out. The prototype machine is then re-configured for 1φ operation and tested at the loading point identified by the model in 1φ operation. The experimental results and the FE results are then compared to highlight the validity of the proposed hypothesis and methodology.

II. MIGRATION FROM 3Φ TO 1Φ OPERATION

While classical SGs working in 1φ operation are not a very common sight, however there have been some cases in literature where this has been investigated [10, 11]. Their proven performance and voltage regulation capabilities make it a good candidate when an efficient, reliable and power quality compliant product is required for electric 1φ energy generation [12]. An optimal way how to do this is as explained in [13], where the idea is to connect two phases in series while leaving the third one open circuited, in order to exploit most of the copper material already available within the slots. With this configuration, the 1φ output power \( P_{1φ} \) is given by the product of the line-to-line voltage and the current flowing inside the 2 connected phases. Thus, the ratio between the 3φ power \( P_{3φ} \) and \( P_{1φ} \) can be written as in (1).  

\[
\frac{P_{1φ}}{P_{3φ}} = \frac{1}{\sqrt{3}} = 0.578 \quad (1)
\]

When it is assumed that the machine design features allow for equal losses in the stator windings for 1φ and 3φ cases, the current ratio shown in (2) would then be feasible and thus the power ratio is as given in (3).

\[
\frac{I_{1φ}}{I_{3φ}} = \frac{\sqrt{3}}{\sqrt{2}} = 1.225 \quad (2)
\]

\[
\frac{P_{1φ}}{P_{3φ}} = \frac{V_{lin}I_{1φ}}{\sqrt{3}V_{lin}I_{3φ}} = \frac{1}{\sqrt{2}} = 0.717 \quad (3)
\]

In (2) and (3), \( V_{lin} \) is the line-to-line voltage and \( I_{3φ} \) and \( I_{1φ} \) are the output currents for the 3φ and 1φ conditions, respectively. Having given the basic relationships between 3φ and 1φ a fundamental step in this transformation process consists in determining the value of \( I_{1φ} \) needed to feed different loads while keeping the output voltage constant. Starting from the BH characteristic of the laminations used for the stator and rotor cores and given the geometrical dimensions, it becomes possible to calculate the magneto-motive-force (mmf) drops along the main flux lines. In Fig. 2, the Arnold-Blondel diagram can be observed, where \( \Phi_M \) is the magnetization flux, \( \Phi_f \) is the excitation flux, \( L_dI_d \) and \( L_qI_q \) are the d-axis and q-axis fluxes.

![Arnold-Blondel diagram of salient pole wound rotor SG](image)

The d- and q-axis currents \( I_d \) and \( I_q \) can be calculated as in (4) and (5) respectively. Then, the no-load electromotive force (emf) value of the unsaturated machine \( E_{gu} \) can be determined as in (6).

\[
I_d = I_s \sin(\delta + \varphi) \quad (4)
\]

\[
I_q = I_s \cos(\delta + \varphi) \quad (5)
\]

\[
E_{gu} = V_S + jX_q I_q + jX_d I_d \quad (6)
\]

In (4)-(6), \( X_q \) and \( X_d \) are the unsaturated reactances of q- and d-axis respectively, \( V_S \) is the stator voltage vector, \( \delta \) is the angle between \( E_{gu} \) and \( V_S \), while \( \varphi \) represents the angle between \( V_S \) and \( I_s \). It becomes now possible to determine the value of the mmf that needs to be supported by the rotor field when the machine is unsaturated. The detailed analytical calculation of all the values of the ampere-turns is shown in [7] and here the final expression is only provided in (7). Here, it can be noticed that the total 1φ and 3φ ampere-turns, \( F_{tot-1φ} \) and \( F_{tot-3φ} \), are related through the constant value equal to \( \sqrt{3} \). This same relationship can be then written between the 1φ and the 3φ field currents.

\[
F_{tot-1φ} = \frac{F_{tot-3φ}}{\sqrt{3}} \quad (7)
\]

Having proven that the field winding current needed for the 1φ operation (when 2 phases are series-connected and 1 phase disconnected) and the line-to-line voltage in 1φ corresponds the phase-to-neutral voltage in 3φ) is \( \sqrt{3} \) smaller than that necessary for the corresponding 3φ operation this scaling factor can be employed to analyse the machine operation at different 1φ loading conditions. It is worth to remark that in this case the line-to-line voltage is \( \sqrt{3} \) smaller compared with the 3φ one in star connection. However, the experimental campaign carried out within this paper keeps the single-phase output voltage at 400V.
III. THE CONSIDERED SG PLATFORM

As mentioned above, this work adopts an off-the-shelf, 400 kVA, salient pole SG as a case study platform. A picture of the machine is shown in Fig. 3, and its main operational parameters and specifications are given Table I.

![Fig. 3. The considered 400 kVA synchronous generator.](image)

| Machine Parameter       | Parameter Value |
|-------------------------|----------------|
| Rated apparent power    | 400 kVA        |
| Rated voltage           | 400 V          |
| Power factor            | 0.8            |
| Frequency               | 50 Hz          |
| Number of poles         | 4              |
| Number of slots         | 48             |
| Outer diameter          | 500 mm         |
| Axial length            | 500 mm         |

The stator winding of the machine has a double-layer structure and features a shortened pitch of 1/3-rd of the pole pitch to remove the 3rd order harmonics. The machine has 2 circuits in parallel on the stator winding, each of them characterized by 8 coils. Another major design feature is the stator slot skewing [14] to attenuate the slotting harmonics. The rotor is a salient-pole one and is equipped with 6 damper bars, implemented symmetrically per pole [15]. All these characteristics can be observed in the 2D cross-section of the machine shown in Fig. 4, where one of the stator phases is highlighted to show the winding configuration.

![Fig. 4. 2D cross-section of the studied SG.](image)

A FE model of this machine was built and validated against experimental results obtained on the prototype. The full operational analysis of the machine and the validation of the FE model is presented in [7]. To replicate these analyses here would go beyond the scope of this paper, however, since the work in this paper relies heavily on the loss characteristics of this machine, then it was felt important to include the loss analysis of the machine. Figures 5 and 6 give the copper and the iron loss values of the SG under several loading conditions and power factors, respectively. These figures compare the results of the FE model shown in Figure 4 against the experimental measures on the machine shown in Fig. 3. A perfect match between FE and the experimental copper losses can be observed in Fig. 5, while an error of ≈10% is found in terms of iron losses, as seen in Fig. 6. In particular, to be coherent with the experimental tests [16], this error is calculated at no-load. The rotor, stator and damper cage losses are separately evaluated via FE analysis as a physical segregation of the experimental iron losses is virtually impossible.

![Fig. 5. FE vs. experimental copper losses at different loadings and power factor values.](image)

![Fig. 6. FE vs. experimental iron losses at different loadings and power factor values.](image)

At full-load (0.8 power factor and 100% loading), the total copper and iron losses of the machine are 18 kW and 5.3 kW respectively. These values of loss obtained by FE and validated experimentally will then be used in the next section as the main constraint to the SG operating in a 1Φ configuration. The maximum 1Φ loading that the machine can supply for the same amount of losses will be found and the machine operated at this loading point.

IV. SG OPERATING IN 1Φ

The FE model shown in Fig. 4 is modified to operate in 1Φ mode. This is done by modifying the stator circuit connections to the configuration shown in Fig. 1, where 2 phases are in series (A and C in the figure) and connected through a purely resistive load (i.e. unity power factor), while the third is left disconnected. As described above, the hypothesis behind this paper is that the 1Φ operation of a classical 3φ SG can be enhanced if the main limiting factor is considered to be the losses in the damper cage winding. However, as the first stage of the analysis, the
machine is investigated for the theoretical 1φ operation, i.e. the model is first run at the rated 1φ operation, as obtained from (1). The expectation here is that the power performance will be good, but the losses in the damper cage winding due to the unbalanced currents will be excessively high. For the model to run with a loading condition as achieved by (1), then a resistive load that represents this loading point is determined and implemented within the FE model. This loading point requires a field current that is \( \sqrt{3} \) less than the rated 3φ field current. This is in line with the analytical description of 1φ operation given in Section II.

Table II shows the results of the model operating at this point, while Fig. 7 illustrates the output voltage and current waveforms registered on the load [17].

Table II

| Component | Value |
|-----------|-------|
| \( V_{rms} \) | 401.1V |
| \( I_{rms} \) | 577.1 A |
| \( P \) | 231 kW |
| \( I_{1-phase} \) | 28.9 A |

For this operating condition, Table III tabulates only the losses induced inside the bars of one of the salient poles (given the odd symmetry characterizing the machine). A map of the field lines’ distribution and of the current density inside the bars is plotted in Fig. 8, where the non-uniform current density distribution within the bars can be observed. From Table III, it can be noticed that the total damper cage loss for this operating 1φ condition amounts to \( \approx 7.35 \) kW which as expected, is actually one order of magnitude higher than the value (i.e. \( \approx 600 \) W) found under the rated full-load 3φ operation (see Fig. 6). This confirms that this 1φ loading condition is not suitable for the machine and therefore the FE model must be used to identify the loading condition that results in a similar amount of losses in the damper cage winding for 1φ and 3φ operation.

Table III

| Bar | Losses [W] |
|-----|------------|
| 1.1 | 270        |
| 1.2 | 149        |
| 1.3 | 123        |
| 1.4 | 92         |
| 1.5 | 152        |
| 1.6 | 1051       |

To find the optimal loading condition, the FE model is used to run various loading conditions. The loading values are chosen according to the available experimental platform (see next section). In Fig. 9, the field current vs. the loading level (at rated output line-to-line voltage) is provided. Table IV gives the value of the 3φ and 1φ losses in the damper cage and the total losses of the machine at different power ratings, evaluated via the FE model described above. From the table, it can be noticed that for higher values of loadings, the damper cage loss becomes more dominant for the 1φ operation, as expected.

Table IV

| Power [kW] | 1φ Damper cage Loss [W] | 1φ Total Losses [W] | 3φ Damper loss [W] | 3φ Total losses [W] |
|------------|-------------------------|---------------------|--------------------|---------------------|
| 4.63       | 212                     | 2778                | 204                | 2624                |
| 9.26       | 218                     | 2786                | 206                | 2900                |
| 16.20      | 236                     | 2889                | 217                | 3043                |
Using Table IV, then it can be identified that the losses inside the damper cage at 1φ operation are similar to those induced at full load in 3φ conditions (see Fig. 6), when the load is at 41.67 kW. Having identified the most suitable 1φ load condition, then the next section is focused on validating the results from the 1φ model by comparison against experimental measurements performed on a 1φ version of the case study machine.

V. EXPERIMENTAL RESULTS

The 400 kVA generator shown in Figures 2 and 3 is modified to operate in 1φ operation, as in Fig. 1. This is achieved quite simply by reconfiguring the winding terminals of the machine in the desired configuration as explained in Section I, i.e. with phase A and C connected in series. With the machine configuration in place, then a testing regime aimed at covering the same loading conditions as given in Table IV for the FE model are done experimentally. The SG field current is provided by a DC power supply in current-mode control and “manually” adjusted to keep the output terminal voltage equal to its rated value of 400 V while the load is varied. The stator terminals are connected to a purely resistive load bank, remotely controllable for modifying the loading condition from 4.63 kW and 50.93 kW. Table V shows a comparison between FE and experimental results relative to the voltage and current values at different loading operations. A very good match can be observed at the various loading conditions investigated. Given that the main objective is that of proving the concept on the established optimal loading of 41.67 kW, the copper and iron losses are reported in Table VI at this specific SG 1φ loading operation. The iron losses are considered equal to the value shown in Fig. 6, as the standard test procedure [16] used to determine them assumes a constant value for the operating loadings of the SG. Since the damper cage losses determination is a very difficult task to perform experimentally, they are taken equal to the values obtained via the FE model (619 W). This is done to 1) fairly compare the FE and experimental results at 1φ operation and 2) to prove that the overall losses produced in 1φ condition (at 41.67 kW) can be safely sustained by the machine and most importantly by the damper winding.

It can be observed from the comparison between the total losses of Table IV and Table VI, at 41.67 kW, that there is an error difference of 11.5%. This highlights the excellent similarity between the predicted and measure results, even when considering the notoriously difficult task of predicting losses accurately. To further strengthen these concepts, thermal steady state measurements were carried out to verify that the rotor temperatures do not exceed the rated limits, when the machine operates at the identified 1φ loading level. Besides the thermocouples located on the SG stator, a number of additional temperature sensors (6 along the active sides and 2 onto the end parts of the rotor field winding – this is done for 2 salient poles) were located onto the rotor. A set of acquisition devices (yoyos) mounted on the machine shaft and thus synchronously rotating with the machine were used for reading the rotor temperatures. In Fig. 10, the yoyos used for such purpose are shown.

![Fig. 10, yoyos log set-up for rotor temperature measurement.](image)

The experimental tests were performed running the machine in 1φ configuration with the resistive load bank set at 41.67 kW and observing that after 6 hours (i.e. the time needed to reach the thermal steady-state) the rotor temperatures raised up to 80°, which is well below the thermal limit specified in the machine datasheet (i.e. 130°). This concept can be seen in Fig. 11, where the trend of the rotor temperatures is plotted against the core length. Due to the location of the cooling fan, whose equivalent position is on the negative values of the x-axes of the figures above, the hot spot is decentralized from the center of the machine core (250 mm) [18, 19]. The results above demonstrate that the considered SG is able to safely operate in 1φ conditions when supplies loads of 41.67 kW.

| Load Level [kW] | Current [A] | Voltage [V] |
|----------------|-------------|-------------|
|                | FE          | Exp.        | FE          | Exp.        |
| 4.63           | 11.32       | 11.58       | 409         | 400         |
| 9.26           | 22.75       | 23.15       | 407         | 400         |
| 16.20          | 39.6        | 40.5        | 410         | 400         |
| 20.83          | 51.5        | 52.08       | 405         | 400         |
| 25.46          | 62.8        | 63.65       | 406         | 400         |
| 30.09          | 75.6        | 75.23       | 398         | 400         |
| 34.72          | 87.1        | 86.8        | 399         | 400         |
| 41.67          | 103.91      | 104.18      | 401         | 400         |
| 46.30          | 117.21      | 115.75      | 395         | 400         |
| 50.93          | 126.07      | 127.33      | 404         | 400         |

| Load [kW] | Copper losses [W] | Iron losses [W] | Bar losses [W] | Total losses [W] |
|-----------|-------------------|-----------------|----------------|------------------|
| 41.67     | 450               | 3850            | 619            | 4919             |

TABLE V

**MACHINE CURRENT AND VOLTAGE VALUES CALCULATED WITH EXPERIMENTAL TESTS**
VI. CONCLUSION

The aim of this paper is to enhance the performance of an off-the-shelf, 3-phase, 400 kVA salient-pole synchronous generator when operating in single-phase. This particular unbalanced operation is critical from a thermal management perspective, due to the negative sequence field inducing very high currents in the machine damper winding. This work first presents a full experimental validation of the FE model purposely built to analyse the 3-phase operation of the considered generator. The analytical background behind the machine operational switch from 3-phase to 1-phase is then investigated. The validated models are then used to study the single-phase operation. A most suitable single-phase loading is found, based upon the concept of maintaining the damper cage loss equal to the value registered at rated, full-load three-phase condition. Experimental tests have been finally performed at the optimal loading of 41.67 kW, at 400 V and unity power factor. Also the rotor temperature profiles has been registered during this test showing a safe operation of the machine. The methods and the findings detailed in this paper have proven that an optimal utilization of 3-phase synchronous generators operating at 1-phase is achievable without relying upon simplified and/or semi-empirical considerations.

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