Effect of phosphate and temperature on force exerted by white muscle fibres from dogfish

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Abstract Effects of Pi (inorganic phosphate) are relevant to the in vivo function of muscle because Pi is one of the products of ATP hydrolysis by actomyosin and by the sarcoplasmic reticulum Ca\(^{2+}\) pump. We have measured the Pi sensitivity of force produced by permeabilized muscle fibres from dogfish (Scyliorhinus canicula) and rabbit. The activation conditions for dogfish fibres were crucial: fibres activated from the relaxed state at 5, 12, and 20°C were sensitive to Pi, whereas fibres activated from rigor at 12°C were insensitive to Pi in the range 5–25 mmol l\(^{-1}\). Rabbit fibres activated from rigor were sensitive to Pi. Pi sensitivity of force produced by dogfish fibres activated from the relaxed state was greater below normal body temperature (12°C for dogfish) in agreement with what is known for other species. The force-temperature relationship for dogfish fibres (intact and permeabilized fibres activated from relaxed) showed that at 12°C, normal body temperature, the force was near to its maximum value.

Keywords Phosphate · Temperature · Permeabilized muscle · Force

Introduction

Intact muscle fibres from dogfish have been used to investigate the mechanics and energetics of contractions that mimic in vivo performance (Curtin and Woledge 1991, 1993a, b, 1996; Lou et al. 1997, 1998a, b, c, 1999, 2000, 2002a, b; Curtin et al. 1997, 1998). Our experiments on intact and permeabilized dogfish fibres give data on force production, turnover of both the physical energy (heat and mechanical work) by intact fibres, and chemical energy (from ATP hydrolysis) during isometric contraction (West et al. 2004). A kinetic model of the crossbridge cycle was devised that accounted for the main features of the results from both intact and permeabilized fibres including time courses of force production and inorganic phosphate (Pi) produced by the actomyosin (AM) ATPase. This evidence suggested that force production by intact and permeabilized dogfish fibres is rather insensitive to [Pi], which contrasts with the extensive body of evidence from experiments on muscle fibres from other animals (Brandt et al. 1982; Altringham and Johnston 1985; Brozovich et al. 1988; Cooke et al. 1988; Godt and Nosek 1989; Pate and Cooke 1989; Dantzig et al. 1992; Pate et al. 1998; Coupland et al. 2001; Debold et al. 2004, 2006; Caremani et al. 2008), and is believed to be due to shifting some of the actomyosin product complex (AM.ADP.Pi) from a high force to a low force state(s). See the recent review by Cooke (2007). This raises the question of whether dogfish fibres are genuinely different from those of other species, or whether some aspect of our experimental conditions caused the dogfish fibres to be insensitive to Pi. Thus we have directly tested the effect of Pi on force using the usual protocol for such experiments (Ca\(^{2+}\) activate from relaxed) at a range of temperatures, and also using an activation protocol in which, like that used by West et al. (2004), the
fibre is activated from the rigor state. The effect of temperature on force produced by intact fibres from dogfish was also tested.

Materials and methods

Dogfish

Dogfish (*Scyliorhinus canicula*, L.) were maintained in re-circulated artificial seawater at 12°C, the temperature of the natural environment for dogfish, and fed chopped mackerel. Fish were held in a cylindrical aquarium (1,000 l) subjected to 12-h light: 12-h dark cycle. The fish were killed by a blow to the head followed by destruction of the brain and spinal cord in accordance with Schedule 1 of the UK Animals (Scientific Procedures) Act 1986. Slices of white visceral cavity. The slices were stored at 5°C in saline containing (mmol l⁻¹): NaCl, 292; KCl, 3.2; MgSO₄, 1.0; Na₂SO₄, 1.6; NaHCO₃, 5.9; CaCl₂, 5.0; urea, 483; and 1.5 mg l⁻¹ of tubocurarine.

Intact fibres

Four fibre bundles were used to measure the effect of temperature (2–20°C) on isometric tetanus force. The methods were similar to those used previously (Lou et al. 2002b) and are described only briefly here. Bundles (4–6 fibres) were dissected and platinum foil clips were attached to the myosepta at the ends of the fibre bundle. The clips were used as stimulating electrodes. At 12°C, the stimulus strength was adjusted to give a maximal twitch response. Brief tetani (0.2 s at 35 Hz) at optimum stimulus strength were used to find the fibre length optimum for isometric force development (L₀). In all subsequent trials fibre length remained at L₀. At each temperature maximal stimulus strength and the stimulus frequency required for a fused tetanus were established. Tetanus duration was adjusted to be sufficient for plateau force to be reached; plateau force is reported. There was a 3-min rest period between tetani, and at least 30 min between tests at different temperatures.

Permeabilized fibres

Bundles of 10–20 fibres, with segments of myosepta attached at each end, were dissected from the slices (West et al. 2004). Fibres were permeabilized by 30 min immersion in ice-cold relaxing solution (Table 1) containing 1% (vol/vol) Triton X-100. The myosepta were removed and a single fibre segment about 4 mm in length was obtained from the bundle; aluminium foil T-clips were then attached to the ends of the preparation.

Rabbit permeabilized fibres

New Zealand White rabbits (>5 kg) were sacrificed with an overdose of pentobarbital in accordance with Schedule 1 of the UK Animals (Scientific Procedures) Act 1986. Bundles of fibres (1–2 mm diameter, 4–5 mm length) were dissected from the psoas major and tied in situ to wood applicator sticks to preserve their in vivo length. Fibres were permeabilized with glycerol as described by Thirlwell et al. (1994) and stored at −20°C for up to 6 weeks before use. For each experiment a segment of a single fibre was isolated from the bundle in relaxing solution (Table 1B) at 5°C. Aluminium foil T-clips were then attached to the ends of the fibre segment.

Experiments on permeabilized fibres

Force was measured by an AE 801 transducer (SensoNor, Horten, Norway). The fibre was mounted via the T-clips between the force transducer and a fixed hook. Once mounted, the dogfish fibres were treated at 12°C, and rabbit fibres at 20°C, for between 30 and 45 min with 0.5–1.0% (vol/vol) Triton X-100 in relaxing solution to remove as much as possible of any remaining membrane fragments and sarcoplasmic reticulum ATPase activity. The fibre was returned to relaxing solution and the striation spacing was adjusted to between 2.35 and 2.45 μm. Striations were photographed through a X40/0.75 w objective lens and measured using custom-designed software. The fibre diameter was measured with an eyepiece graticule (X40/0.75 w objective lens) and fibre segment length with an eyepiece graticule in a stereomicroscope. The dogfish fibres are much larger than the rabbit fibres (cross-sectional areas 24,981 ± SEM 925 μm², n = 41 and 5,646 ± SEM 295, n = 34, respectively).

Activation protocol 1: Dogfish fibres at 5, 12, and 20°C

Fibres were transferred from pre-activating solution to activating solution at 5°C for 8 s, then to activating solution at 12 or 20°C for 4 s, and finally to relaxing solution at 12 or 20°C. This protocol was repeated three times on each fibre with the order of the added [Pi] (mmol l⁻¹) being for half of the fibres: 0, 20, 0, and for the other half: 20, 0 and 20. Twenty fibres were tested at 5 and 12°C. An additional ten fibres were tested at 5 and 20°C. See Table 1A for solutions and Fig. 1 for example records. The average peak force observed in these experiments with 0 added Pi was 285 ± SEM 7.7 kPa (n = 20 fibres) when the higher temperature was 12°C and 277 ± SEM 8.9 kPa (n = 10 fibres) for 20°C.
Activation protocol 2. Dogfish fibres at 12°C, and rabbit fibres at 20 and 35°C

Fibres were transferred from relaxing solution through the following sequence of solutions: pre-rigor, Ca²⁺-free rigor, and Ca²⁺-rigor for about 5 min each. Following this, the fibre was transferred to activating solutions with added [Pi] (mmol l⁻¹) 0, 5, 10 and 20 for about 40 s each and then transferred to post-activation relaxing solution. The order in which the different [Pi] were used was varied between experiments. See Table 1B for solutions and Fig 2 for example records.

When a fibre was used for a second or third series of activations, it remained in the post-activation relaxing solution for a minimum period of 10 min before continuing through the sequence: pre-rigor, etc. To minimize exposure to 35°C where this was the test temperature, the relaxing, pre-rigor and Ca²⁺-free rigor solutions were at 20°C.

The force values reported in the Results are based on the difference between the force at the end of the period in each activating solution and that in the post-activation relaxing solution (see Fig. 2). Ranatunga (1994) has shown that Ca²⁺-independent force can develop at temperatures above 25°C, but at 35°C and the sarcomere lengths used here this force is small (<5%) compared to Ca²⁺-dependent force. To take account of variation between force-producing capacities of the fibres due to differences in size, each force measurement in a record (for example, each of the four measurements in the record shown in Fig. 2a) was expressed relative to the mean of these four force measurements. The two-way regression analysis of these size-independent force values vs log₁₀[Pi] and activation order was made for each set of data, dogfish, rabbit at 20°C, and rabbit at 35°C. The constants (i, s and o) in the following equation were adjusted to give a best fit to the force values by minimizing the sum of the squared difference between the observed and calculated (fy) force values:

\[ f = a + (s \times \log_{10}[Pi]) + (o \times n) \]

where \( \log_{10}[Pi] \) is the log₁₀ of the Pi concentration in mmol l⁻¹, and n is the number of the activation, for example, 1, 2, 3 or 4 in the series. The results of the regression are shown in Table 2 and were used to remove the variation in force due to variation in activation number.

### Table 1 Solution composition for experiments on permeabilized fibres

#### A. Protocol 1

|          | Relax | Pre-activ | Activ |
|----------|-------|-----------|-------|
| Free Ca²⁺| 0     | 0         | 0.032 |
| Total EGTA | 25    | 0.1       | 25    |
| Total HDTA | 0     | 24.9      | 0     |
| Total added Pi | 0 | 0         | 0 or 20 |

#### B. Protocol 2

|          | Relax | Pre-rigor | Ca-free rigor | Ca rigor | Activ | Post-activ relax |
|----------|-------|-----------|---------------|----------|-------|-----------------|
| Free Ca²⁺| 0     | 0         | 0             | 0.032    | 0.032 | 0               |
| MgATP    | 5     | 0.2       | 0             | 0        | 5     | 5               |
| PC       | 0     | 0         | 0             | 20       | 20    | 0               |
| Total added Pi | 0 | 0         | 0             | 0, 5, 10 or 20 | 0 |
| BDM      | 0     | 10        | 10            | 0        | 0     | 0               |
| CK       | 0     | 0         | 0             | 863      | 863   | 0               |
| Apyr     | 0     | 0         | 0             | 33       | 0     | 0               |
| IS       | 200   | 200       | 200           | 300      | 300   | 300             |

Relax, relaxing solution; Post-activ relax, post-activation relaxing; TES, N-tris[(Hydroxymethyl)methyl]-2-aminoethanesulfonic acid; EGTA, 1,2-Di(2-aminoethoxy)ethane-N,N',N'-tetra-acetic acid; PC, phosphocreatine; HDTA, N-(2-Hydroxyethyl) ethylenediamine-N,N',N'-triacetic acid; BDM, 2,3-butanedione 2-monoxime, tri-sodium salt; CK, creatine phosphokinase; Apyr, apyrase; IS, ionic strength. Concentrations in mmol l⁻¹ except CK and Apyr, which are U ml⁻¹.

Protocol 1: For experiments on dogfish fibres at 5, 12 and 20°C. All solutions contained (mmol l⁻¹): MgATP 3.5; free Mg²⁺ 2.0, PC 10, glutathione 10, glycerol-2-phosphate 15, CK 863 U ml⁻¹. pH 7.1. Ionic strength was adjusted to 300 mmol l⁻¹ with K-propionate.

Protocol 2: For experiments on dogfish fibres at 12°C. All solutions contained (mmol l⁻¹): free Mg²⁺ 2.0, total EGTA 30, glutathione 10, TES 60, pH 7.25. Ionic strength was adjusted with K-propionate. For experiments on rabbit fibres at 20 and 35°C, the solutions were the same as dogfish at 12°C except total EGTA 20, PC 10, pH 7.15 at 20°C, pH 6.96 at 35°C, and IS 190.
while leaving the effect of variation in [Pi]. In other words, each force value was adjusted to what it would be for activation number = 1.

The average peak force observed in these experiments was 143 ± SEM 14 kPa (n = 18 fibres) for dogfish fibres at 12°C and 185 ± SEM 10 kPa (n = 19 fibres) for rabbit fibres at 20°C and 145 ± SEM 13 kPa (n = 18 fibres) at 35°C.

**Background Pi**

The background [Pi] is concentration present when no Pi has been added to the activation solution. It is the sum of Pi contamination and Pi accumulation due to actomyosin ATPase. See Table 3 for the total background Pi and its components.

**Pi contamination**

The free Pi content of phosphocreatine (PC) and of glycerol-2-phosphate (G2P) were assayed using N-(2-[1-
maleimidyl[ethyl]-7-diethylamino-coumarin-3-carboxamide phosphate binding protein (MDCC-PBP, West et al. 2004 and references therein). Standard curves were made using dilutions of KH$_2$PO$_4$. MDCC-PBP fluorescence was measured using a CaSpectrofluorometer (SPEX FluoroMax-3, HORIBA Jobin–Yvon). The results showed that the Pi contamination in PC was 5.74% and in G2P was 0.694%.

**Pi produced during contractions**

In the experiments with permeabilized fibres Pi is produced by hydrolysis of ATP during contraction and some of it diffuses out of the fibre. We used the diffusion model described in the legend of Table 4 to calculate the net effect of Pi production by ATP hydrolysis in the fibres and Pi diffusion out of the fibres.

**Table 2** Regression of force vs. log$_{10}$ [Pi] and activation number

| Preparation | T (°C) | $i$ (+SE) | $s$ (+SE) | $P$ (+SE) | $o$ (+SE) | $d_f$ |
|-------------|--------|-----------|-----------|-----------|-----------|-------|
| Dogfish     | 12     | 1.127     | 0.056     | <0.001    | 0.039     | 0.862 |
| Rabbit      | 20     | 1.202     | 0.027     | <0.001    | 0.023     | <0.001|
| Rabbit      | 35     | 1.205     | 0.030     | <0.001    | 0.027     | <0.001|

Force = $i + (s \times \log_{10}[Pi]) + (o \times n)$, where force = force/mean force for all activations of that preparation in the same series (see Fig. 2). $i$ = intercept; $s$ = slope = Dforce/Dlog$_{10}$ [Pi]; $o$ = slope = Dforce/Dactivation, where activation is the number (n) of the activation, 1, 2, etc., in the series (see Fig. 2). $P$ is the probability for null hypothesis that the intercept or slope value is equal to zero. Degrees of freedom = $df$ = number of force values - 1

**Table 3** Background [Pi]

| Fibre source | Activation protocol | T (°C) | [Pi] when 0 added Pi |
|--------------|---------------------|--------|---------------------|
|              |                     |        | From PC (mmol l$^{-1}$) | From G2P (mmol l$^{-1}$) | Net from AM-ATPase (mmol l$^{-1}$) | Total background[Pi] (mmol l$^{-1}$) |
| Dogfish      | 1                   | 5      | 0.574               | 0.104                | 1.348                        | 2.026                       |
| Dogfish      | 1                   | 12     | 0.574               | 0.104                | 1.818                        | 2.496                       |
| Dogfish      | 1                   | 20     | 0.574               | 0.104                | 3.036                        | 3.714                       |
| Dogfish      | 2                   | 12     | 1.147               | –                    | 3.981                        | 5.128                       |
| Rabbit       | 2                   | 20     | 0.574               | –                    | 0.751                        | 1.325                       |
| Rabbit       | 2                   | 35     | 0.574               | –                    | 3.460                        | 4.034                       |

Background Pi is that present in activation solution to which no Pi has been added. Activation protocol 1 and 2 see text for details. T is temperature. Sources of Pi: PC is phosphocreatine added to activation solution, G2P is glycerol-2-phosphate added to the activation solution, and net AM-ATPase is the net effect of Pi from the actomyosin ATPase and diffusion as described in Table 4. Total background is the sum of Pi from PC, G2P and net AM-ATPase

**Table 4** Pi from net effect of actomyosin ATPase and diffusion

| Fibre source | Activation protocol | T (°C) | AM-ATPase (s$^{-1}$) | D (μm$^2$ s$^{-1}$) | [Pi] (mmol l$^{-1}$) | Condition |
|--------------|---------------------|--------|---------------------|---------------------|---------------------|-----------|
| Dogfish      | 1                   | 5      | 2.4 (1)             | 184.0               | 1.348               | (a)       |
| Dogfish      | 1                   | 12     | 6.0 (2)             | 221.3               | 1.818               | (b)       |
| Dogfish      | 1                   | 20     | 17.3 (1)            | 273.0               | 3.036               | (c)       |
| Dogfish      | 1                   | 12     | 6.0 (2)             | 221.3               | 3.981               | Equilibrium |
| Rabbit       | 2                   | 20     | 5.9 (3)             | 273.0               | 0.751               | Equilibrium |
| Rabbit       | 2                   | 35     | 40.3 (4)            | 405.0               | 3.460               | Equilibrium |

AM-ATPase is rate of Pi production by actomyosin (units: mol Pi. mol myosin$^{-1}$. s$^{-1}$). Sources: (1) calculated from dogfish 12°C value using $Q_{10}$ 3.75, the average from Hill and Woledge (1962) and Homsher and Keen (1978). (2) West et al. (2004). (3) Hilber et al. (2001). (4) Calculated from the rabbit 20°C value using $Q_{10}$ 3.6 from Hilber et al. (2001). D is the diffusion coefficient for Pi based on value of 210 μm$^2$ s$^{-1}$ at 10°C and $Q_{10}$ 1.3, from Coupland et al. (2001). [Pi] = net [Pi] due to AM-ATPase and diffusion for conditions: (a) 8 s contraction at 5°C; (b) 8 s contraction at 10°C followed by 1 s at 12°C; (c) 8 s contraction at 5°C followed by 1 s at 20°C. The diffusion calculation assumes the fibre radius is divided into 40 shells of equal thickness. Fibre radii were: 89.5 and 86.4 μm for dogfish used in protocol 1 and 2, respectively, and 42 μm for rabbit.
Results

Force produced by permeabilized fibres

Activation protocol 1: Activation from resting state

The example records in Fig. 1 show that force produced by dogfish fibres was influenced by temperature and [Pi]. Force increases abruptly when temperature is increased after 8 s of activation. Force was less in the solution with added Pi (20 mmol l\(^{-1}\), broken lines in Fig. 1) than with no added Pi (full lines). In each experiment there was a repeat test with one of the solutions; the repeat measurements were averaged and then force with 20 mmol l\(^{-1}\) added Pi was expressed relative to force without added Pi. The results from all 30 experiments of this type are summarized in Fig. 3a (open symbols), where the relative force is plotted against the logarithm of the total Pi concentration, that is the background level plus any added Pi (see Methods). The effect of Pi on force is greater at 5\(^\circ\)C than at either 12 or 20\(^\circ\)C; the effect is almost the same at the two higher temperatures.

Activation protocol 2: Activation from rigor

Figure 2 shows example records of force produced by a dogfish fibre during contraction in a series of solutions containing different [Pi]. In Fig. 2a, [Pi] was increased (5.13, 10.12, 15.13, and 25.12 mmol l\(^{-1}\)) progressively (order number: 1–4). In Fig. 2b, [Pi] was progressively decreased. The records for rabbit fibres were qualitatively similar to those shown in Fig. 2. To examine the effect of [Pi] on force, the relationship of force to both log\(_{10}\) [Pi] and order number was investigated by two-way regression analysis. The results in Table 2 show that force produced by dogfish fibres did not vary significantly with variations in log\(_{10}\) [Pi] (\(P = 0.862\)), whereas force did vary inversely with order number (\(P < 0.001\)). Force produced by rabbit fibres varied inversely with both log\(_{10}\) [Pi] and order number; these relationships were statistically significant at both 20 and 35\(^\circ\)C (all \(P\) values \(\leq 0.002\)). In order to compare the results with those from activation protocol 1 the forces were adjusted to order number = 1 to remove the effect of variation in the order of presentation of [Pi]. In addition, force was expressed relative to the value with no added Pi. The results are summarized in Fig. 3a, b. Force production by dogfish fibres activated from rigor (activation protocol 2, closed symbols, Fig. 3a) is not affected by increasing [Pi], in contrast to the results for activation from the resting state (activation protocol 1, open symbols). Figure 3b shows that force production by rabbit fibres activated from rigor (black symbols) was depressed by [Pi] at both 20 and 35\(^\circ\)C.

Effect of temperature on force produced by intact fibres from dogfish

Figure 4b (closed symbols) shows force produced by four bundles of intact fibres from dogfish tested in the range 2–20\(^\circ\)C. Temperature strongly influenced force during isometric tetani at \(L_0\), but the dependence of force on temperature was non-linear. Reducing temperature below...
12°C, the normal body temperature for dogfish, had a larger effect on force than increasing temperature did. Permeabilized dogfish fibres activated from the relaxed state (activation protocol 1) also show the effect of temperature on force. The results are included in Fig. 4b (open squares) and were very similar to those from intact fibres.

Discussion

Figure 3 shows how Pi influences force produced by dogfish (Fig. 3a) and rabbit (Fig. 3b) fibres. The dogfish fibres when activated from the relaxed state (activation protocol 1, open symbols) showed a clear sensitivity to Pi, which is greatest at the lowest temperature tested (5°C). However, when dogfish fibres were activated from rigor (activation protocol 2, closed symbols Fig. 3a) force is insensitive to [Pi], which is clearly different from the rabbit results obtained with the same activation protocol (closed symbols Fig. 3b). For comparison some of the results of Coupland et al. (2001) for rabbit fibres have been added to Fig 3b. In our experiments the effect of Pi on force is less than found by Coupland et al. (2001). The differences are likely to be due to the state of the fibre when activation was initiated because in our activation protocol 2 experiments the fibres were activated from rigor, whereas Coupland et al. (2001) activated their fibres from the relaxed state.

Our results for the rabbit fibres agree with the numerous reports that skinned fibres from many animal species produce less force the higher the [Pi]; for example, rabbit (Brandt et al. 1982; Brozovich et al. 1988; Godt and Nosek 1989; Pate and Cooke 1989; Millar and Homsher 1990; Dantzig et al. 1992; Potma et al. 1995; Potma and Stienen 1996; Pate et al. 1998; Coupland et al. 2001; Caremani et al. 2008), rat (Fryer et al. 1995; Debold et al. 2006), frog (Brozovich et al. 1988; Stienen et al. 1990), Xenopus (Stienen et al. 1999), insect: (Ruegg et al. 1971) and references therein. The force vs. [Pi] relationship of rabbit (Coupland et al. 2001) and rat (Debold et al. 2006) fibres has been investigated over a range of temperatures up to 30°C. For both species force produced at maximum Ca2+ activation is most affected by [Pi] at low temperature.

The effects of temperature on the Pi sensitivity of force are shown in Fig. 4a where the slopes of the regression lines from Fig. 3 (Δ force/Δ log [Pi]) are plotted against temperature. It is clear that in both species Pi sensitivity is greater in experiments in which the fibres were activated from the relaxed state (open symbols) than when they were activated from rigor (closed symbols). In both species the results using activation from the relaxed state show the greatest Pi sensitivity at the lowest temperature tested. Figure 4b shows the effects of temperature on force for dogfish intact fibres (closed symbols) and for permeabilized fibres activated from the relaxed state; dogfish (open squares) and rabbit fibres (gray broken line). For the dogfish there is good agreement between the results for intact and permeabilized fibres. It is clear that the shape of the relation is similar for rabbit and dogfish experiments, but the dogfish results lie to the left of the rabbit results by approximately 10°C. Correspondingly, the results for Pi sensitivity in the two species (when activated from the relaxed state) would
be similar if the rabbit results were shifted to the left by 10°C (Fig. 4a). These relationships show that force is relatively insensitive to [Pi] at the physiological temperature of each species (dogfish 12°C and rabbit 39°C). At these temperatures, force is high and thus most crossbridges are in the force-producing states, suggesting that crossbridges in the high force state retain the Pi from ATP splitting and are thus insensitive to [Pi] concentration.

We quantitatively simulated the dependence of force on [Pi] and temperature, extending the qualitative approach used by Coupland et al. (2001). We used the following abbreviated model of the crossbridge cycle, which is similar to that used by Coupland et al. (2001). The model is referred to as “abbreviated” because it includes the minimum states and steps required to simulate our results; there are only three attached states, and only three steps. Step III includes all transitions required to complete the cycle from AM·ADP to AM·ADP·Pi.

Simulations in both Fig. 4a and b were calculated from the reaction scheme:

\[
\text{States 1, 2, 3} \\
\rightarrow \text{AM·ADP·Pi} \leftrightarrow \text{AM·ADP·Pi} \\
\leftrightarrow \text{AM·ADP} + \text{Pi} \\
\text{Steps (III)} = (I) \quad (II) \quad (III)
\]

Parameters used to adjust the kinetic model to fit the different data sets are shown in the table below.

| Activation protocol | K_I (mmol l^{-1}) | ΔH_I (kJ mol^{-1}) | ΔH_{II} (kJ mol^{-1}) |
|---------------------|-------------------|--------------------|----------------------|
| Rabbit 1            | 0.92              | 7.67               | 73                   |
| Rabbit 2            | 1.76              | 12.7               | 52                   |
| Dogfish 1           | 1.3               | 4.9                | 34                   |
| Dogfish 2           | 8.2               | 0.13               | 61                   |

Step I: \( k_{-I} = 135 \text{ s}^{-1} \) at 20°C and has \( Q_{10} = 2.3 \). \( k_{+I} \) is calculated from \( k_{-I} \) and \( K_I \). The table gives the \( K_I \) values at 20°C; values for other temperatures are calculated using the Van’t Hoff equation and \( ΔH_I \) values in the table.

Step II: \( k_{+II} = 1,000 \text{ s}^{-1} \) at 20°C and has \( Q_{10} = 2.3 \). \( k_{-II} \) is calculated from \( k_{+II} \) and \( K_{II} \). The table gives the \( K_{II} \) values at 20°C; values for other temperatures are calculated using the Van’t Hoff equation and \( ΔH_{II} \) values in the table.

Step III: \( k_{+III} \) is calculated from the other rate constants and the rate of ATP turnover shown in Table 4.

State 1 is an attached state that produces no force, and states 2 and 3 are attached states that produce high and equal force, similar to various other models (Dantzig et al. 1992; Coupland et al. 2001; Caremani et al. 2008). Step I, the force-producing step, is endothermic. An increase in temperature increases force (Goldman et al. 1987; Bershitsky and Tsaturyan 2002) by altering the force per attached crossbridge, without increasing the proportion of bridges that are attached (Piazzesi et al. 2003). The Pi release step (II) occurs after force has been developed (step I) (Smith and Sleep 2004).

We have modified the model by constraining it to have the rate of ATP turnover and temperature dependence detailed in Table 4. We found that the fit to our results was improved by making step II endothermic as well as step I. As shown in Fig. 4 the model provides a good simulation of the temperature dependence of the Pi sensitivity of force (Fig. 4a, full lines) and the temperature dependence of force in each species (Fig. 4b, full line and open triangles). The simulation used the rate constants given above.

Although this simple model can explain reasonably well the effects of temperature on force and on Pi sensitivity of force it is unlikely to explain some of the other effects of Pi which have been observed. For example, it has been reported (Potma et al. 1995) that the ATPase rate of rabbit skinned fibres is depressed less than force by increase of [Pi]. Also Caremani et al. (2008) have shown that the stiffness of rabbit permeabilised fibres is reduced by Pi in proportion to force. Caremani et al. present a model, very similar to ours, that can account for the effects of Pi on force and stiffness. However, there is no obvious way in which it can account for the fact that Pi-sensitivity is less at higher temperature. It seems that a more complex kinetic scheme than that proposed by Caremani et al. (2008), or that proposed here, is required to account for the combined effects of Pi and temperature on force, stiffness and ATPase rate. Such a scheme would include an endothermic force-producing step that occurs without a change in the biochemical state of the attached crossbridge, as suggested by Caremani et al. (2008), and by Woledge et al. (2009).

Implications for in vivo function

Our results taken together with those of Coupland et al. (2001) and Debold et al. (2006) suggest that at physiological temperature Pi accumulation has little effect on force production in skinned fibres when maximally Ca^{2+} activated. To the extent that this also applies for intact fibres, the results add to the evidence that very little of the reduction in force during fatigue could be explained by the effects of [Pi] acting alone on the crossbridge cycle itself, by causing a shift to low or non-force producing states. “Acting alone” must be noted because other chemical species change along with Pi even in the very brief contractions that are typical of in vivo function of intact fibres. In addition, activation of the crossbridge cycle by Ca^{2+} is affected by [Pi] (Allen et al. 2008) and thus could reduce force produced by intact fibres, despite having no effect in skinned fibres.
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