Refractive Index Enhancement with Vanishing Absorption in an Atomic Vapor

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Abstract

We report a proof-of-principle experiment where the refractive index of an atomic vapor is enhanced while maintaining vanishing absorption of the beam. The key idea is to drive alkali atoms in a vapor with appropriate control lasers and induce a gain resonance and an absorption resonance for a probe beam in a two-photon Raman configuration. The strength and the position of these two resonances can be manipulated by changing the parameters of the control lasers. By using the interference between these two resonances, we obtain an enhanced refractive index without an increase in the absorption.

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Since the birth of quantum and nonlinear optics, one of the key challenges has been if one can achieve a very large refractive index for a laser beam [1]. A key application of a large refractive index is to optical imaging science. It is well-known that the wavelength of light inside a refractive medium is \( \lambda = \lambda_0 / n \), where \( \lambda_0 \) is the wavelength in free space and \( n \) is the refractive index. A large refractive index, therefore, corresponds to a reduced wavelength inside the medium and enhanced imaging resolution. Another important application of a large refractive index is to optical lithography where the smallest feature size of a lithographic mask is determined by the wavelength of light. A simple and an efficient way to achieve a large refractive index is likely to have significant practical implications since lithographic resolution currently determines the size and the processing power of every semiconductor integrated circuit.

A laser beam which is tuned close to an atomic resonance can experience a large refractive index. As an example, the refractive index for a gas at a pressure of 1 torr can reach values as high as 10. However, such a large index is usually accompanied by large absorption and the effect is not useful. This is because, near an optical resonance, the real and imaginary parts of the optical susceptibility are of the same order. It was first pointed out by Scully that, by using interference in a three state atomic system, it is possible to obtain a large refractive index with negligible absorption [2, 3]. The pioneering work of Scully was extended to different configurations by Fleischhauer and colleagues [4, 5, 6]. Although these ideas were experimentally demonstrated in a Rb vapor cell by Zibrov et al. [7], it has not yet been possible to achieve a refractive index in a vapor that is large enough to be of practical importance. In this work, we report a proof-of-principle experiment that demonstrates a new approach to this long-standing problem [8, 9]. By utilizing the interference of two Raman resonances, we show that the refractive index of a laser beam that is very far detuned from an electronic resonance can be enhanced while maintaining vanishing absorption.

Before proceeding with a detailed description of our experiment, we note that in recent years, a number of counter-intuitive effects in driven atomic systems have been predicted and demonstrated [10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22]. Of particular importance is the demonstration of slow light [12, 13, 14], stopped light [15, 16, 17], fast and backward light [18, 19], and enhanced nonlinearities using Electromagnetically Induced Transparency [20, 21, 22]. Broadly, most of these effects can be thought as engineering the variation (the slope) of the refractive index as a function of frequency. In contrast, our technique allows us
to engineer the actual value of the refractive index while maintaining vanishing absorption to the beam. In this sense, our approach complements the existing techniques in modifying the optical response of an atomic medium.

In our experiment, we follow the suggestion of Yavuz et al. which has recently been extended to high alkali densities by Kocharovskaya and colleagues. The essential features of this idea are presented in Fig. 1. It is well-known that, the interference of the dipole moments of an absorptive resonance and an amplifying resonance can lead to an enhanced refractive index with vanishing absorption. As shown in Fig. 1(a), the most straightforward way to realize such an interference would be to have two different two-level atomic species. In practice, such a multiple two-level atom scheme has not yet been realized since it is difficult to find two different atomic species with very close and easily tunable resonance frequencies. The key idea that we experimentally demonstrate in this work is that such a multiple two-level scheme can be realized by using Raman resonances in far-off resonant atomic systems. As shown in Fig. 1(b), with an atom starting in the ground state $|g\rangle$, a Raman transition involves absorption of one photon and emission of another photon of different frequency such that the two-photon resonance condition is satisfied. By changing the order at which the probe laser, $E_p$, is involved in the process, such a Raman resonance can be made absorptive or amplifying. This approach circumvents the difficulties of the scheme of Fig. 1(a). The two Raman transition frequencies can be arbitrarily different since we have the freedom to choose the frequencies of the control lasers, $E_{c1}$ and $E_{c2}$. Figure 1(c) shows the real and the imaginary parts of the susceptibility for the case of equal strength of the two resonances. The real part of the susceptibility, $\chi'$, and therefore the refractive index, peaks at the point of vanishing imaginary part, $\chi''$.

We demonstrate the scheme of Fig. 1(b) in two isotopes of atomic Rubidium, $^{87}$Rb and $^{85}$Rb. Figure 2 shows the simplified experimental set up and the relevant energy level diagrams. We work with a triple layer magnetically shielded and temperature controlled natural abundance Rb (28% $^{87}$Rb, 72% $^{85}$Rb) vapor cell. The vapor cell is $L = 7.5$ cm long and contains 10 torr of Neon (Ne) as a buffer gas. The temperature of the vapor cell is kept at $T = 90$ degrees Celsius which gives a total atomic density of $N \approx 2.4 \times 10^{12}$ / cm$^3$. We use $F = 2 \rightarrow F = 1$ and $F = 2 \rightarrow F = 3$ hyperfine transitions in $^{87}$Rb and $^{85}$Rb respectively (in ground electronic state $5S_{1/2}$). For Raman transition between the hyperfine states, we utilize far-off resonant excitation through the excited electronic state $5P_{3/2}$ (D2 line) near
FIG. 1: (Color online) The interference of an absorptive resonance and an amplifying resonance can lead to an enhanced refractive index with vanishing absorption. (a) shows the most straightforward way to achieve such an interference. Due to various difficulties, the scheme in (a) is not practical (see text for details). (b) shows an equivalent scheme that we experimentally demonstrate in this work. With an atom starting in the ground state $|g\rangle$, a Raman transition involves absorption of one photon and emission of another photon of different frequency such that the two-photon resonance condition is satisfied. By changing the order at which the probe laser, $E_p$, is involved in the process, such a Raman resonance can be made absorptive or amplifying. (c) shows the real part, $\chi'$, and the imaginary part of the susceptibility, $\chi''$, as a function of frequency. Here, we take the two resonances to be of equal strength with a width of 0.1 MHz and assume the spacing between resonances to be 0.2 MHz.

A wavelength of $\lambda = 780.2$ nm. We drive the two Raman transitions with a weak probe beam, $E_p$, and two strong control lasers, $E_{c1}$ and $E_{c2}$. The frequency differences between respective beams are tuned close to hyperfine transition frequencies, $\omega_p - \omega_{c1} \approx 6.834$ GHz and $\omega_p - \omega_{c2} \approx 3.035$ GHz. The frequency of the probe laser beam, $\omega_p$, is detuned $\approx 16$ GHz.
from the D2 line in $^{87}$Rb.

![Diagram](image_url)

FIG. 2: (Color online) Simplified experimental set-up and the energy level diagram (not to scale) for the two isotopes. The experiment is performed in a magnetically shielded, natural abundance Rb vapor cell. Two optical pumping lasers optically pump the two species to the $F = 2$ hyperfine state in the ground electronic state. With the atoms optically pumped, three experimental laser beams, $E_p$, $E_{c1}$, and $E_{c2}$ drive two Raman transitions, one in each isotope. The interference of these two resonances lead to enhanced refractive index with vanishing absorption. All three laser beams are far-detuned from the single-photon electronic resonance.

We start the experiment by optically pumping both of the atomic species to the $F = 2$ hyperfine state manifold. This is achieved by two optical pumping lasers locked to $F = 1 \rightarrow F' = 2$ transition in $^{87}$Rb and $F = 3 \rightarrow F' = 3$ transition in $^{85}$Rb respectively. Each optical pumping beam has a power of about 0.5 W and is obtained by seeding a semiconductor tapered amplifier with an external cavity diode laser. The optical pumping beams have a
collimated beam radius of \( \approx 3 \) mm and counter-propagate the three experimental beams as shown in Fig. 2(a).

The three experimental beams, \( E_p, E_{c1}, \) and \( E_{c2} \), are derived from a single external cavity master diode laser. The output of this laser is appropriately shifted by three high frequency acousto-optic modulators (AOM) in parallel to produce the desired frequency spacing between respective beams. After the AOMs, the control beams are amplified by tapered amplifiers to achieve the required power levels. The frequency of each of the three laser beams can be tuned by changing the modulation frequency of the AOMs. This set-up gives us complete control over the position of the two Raman resonances when we scan the frequency of the probe laser beam. Further details regarding our laser system can be found in our previous publications [23, 24]. The polarization of the probe beam is linear and orthogonal to the polarization of the two control laser beams. The three beams have a collimated beam waist of \( W_0 = 1.2 \) mm at the vapor cell. The probe laser has an optical power of about 1 mW and is much weaker when compared with the control lasers (\( \approx 100 \) mW each).

We run the experiment in a timing cycle where we optically pump the atoms for about 500 \( \mu s \). We then turn-off the optical pumping beams and turn-on the probe and the control lasers. To avoid undesired time-dynamics due to sharp edges, we turn-on the three beams smoothly over about 10 \( \mu s \) and perform our measurements at the peak of the pulses. After the beams exit the vapor cell, we separate the weak probe beam with a high-extinction polarizer. To determine the gain or the loss on the probe beam, we measure the intensity of the beam at the peak of its spatial profile right after it leaves the vapor cell.

Figure 3 shows the electromagnetically induced gain and absorption resonances on the probe beam and our ability to control these resonances. Here, we measure the peak intensity of the probe beam as a function of the probe laser frequency. The solid line in each plot is a fit to the data that assumes each resonance to be a Lorentzian. When the probe laser is resonant with the \( F = 2 \rightarrow F = 1 \) transition in \( ^{87}\text{Rb} \), there is gain on the beam. When it is resonant with \( F = 2 \rightarrow F = 3 \) transition in \( ^{85}\text{Rb} \), there is loss. By changing the frequencies of the control lasers, we can control the position of these resonances as we scan the frequency of the probe laser beam. In Figs. 3(a) and 3(b), the gain resonance happens before the loss resonance whereas in Figs. 3(c) and 3(d), the situation is reversed.

We proceed with a discussion of the measurement of the refractive index. Due to the
FIG. 3: (Color online) The peak intensity of the probe laser measured after the cell as a function of the frequency of the probe laser. With the control lasers, we induce a gain resonance and an absorption resonance on the probe laser. When the probe laser is resonant with the \( F = 2 \rightarrow F = 1 \) Raman transition in \( ^{87}\text{Rb} \), the beam experiences gain. When it is resonant with \( F = 2 \rightarrow F = 3 \) Raman transition in \( ^{85}\text{Rb} \), the beam experiences loss. By changing the frequencies of the control lasers, we can tune each of the Raman resonances. In plots (a), (b), (c), and (d), the two resonances are spaced by 0.8 MHz, 0.4 MHz, -0.4 MHz, and -0.8 MHz respectively.

Spatial profile of the control lasers, the refractive index enhancement is larger at the center of the probe beam when compared with the wings of the beam. As a result, the probe beam acquires a spatially dependent phase as it propagates through the atomic medium. In essence, the medium acts as a thin lens causing the probe beam to focus or defocus after the cell \([24]\). To measure the electromagnetically induced focusing effect, we measure
the transmission of the probe beam through a 150 \( \mu \text{m} \) wide pinhole placed 2.5 m away from the cell. If the beam focuses (de-focuses), the beam size decreases (increases) and the transmission through the pinhole increases (decreases).

FIG. 4: (Color online) Experimental demonstration of the refractive index enhancement at the point of vanishing absorption. (a) The peak intensity of the probe beam and (b) the transmission through a pinhole as a function of probe laser frequency. The transmission through the pinhole changes as a result of focusing or defocusing of the beam due to spatial dependence of the refractive index. The pinhole transmission and therefore the refractive index is maximized at the point of vanishing absorption. The solid line in (a) is a fit that assumes the two resonances to be Lorentzian. The solid line in (b) is the calculated refractive index change at the peak of the spatial profile based on the fit of (a). We see good qualitative agreement between pinhole transmission data and our calculation.

In Figure 4, we measure the peak intensity of the probe beam simultaneously with the transmission through the pinhole. The pinhole transmission is appropriately normalized to
take into account the gain or absorption of the beam. In essence, the intensity measurement of Fig. 4(a) probes the imaginary part of the susceptibility ($\chi''$) whereas the pinhole transmission measurement of Fig. 4(b) probes the real part of the susceptibility ($\chi'$). For this data, we adjust the control laser frequencies such that the two resonances are separated by 0.2 MHz which is roughly twice the width of each resonance. The pinhole transmission, and therefore the refractive index, is maximized at the point of vanishing gain or loss on the beam. The solid line in Fig. 4(a) is a fit to the data that assumes each resonance to be Lorentzian. The solid line in Fig. 4(b) is the calculated refractive index based on the fit to the data of Fig. 4(a). We see good qualitative agreement between the refractive index calculation and the pinhole transmission data.

Currently, our experiment suffers from an undesired cross-coupling of the two optical pumping processes. The $^{87}$Rb optical pumping laser tries to pump the $^{85}$Rb atoms to the wrong state and vice versa. Due to this cross coupling, our optical pumping efficiency is low and the observed refractive index in our experiment ($\Delta n \approx 10^{-6}$) is about an order of magnitude lower than the ideal limit for our experimental parameters. This problem can be solved by going to a different laser system and pumping both species to their lower energy hyperfine ground states ($F = 1$ in $^{87}$Rb and $F = 2$ in $^{85}$Rb) which we plan to implement in the near future.

One key advantage of our scheme is that by increasing the intensities of the control lasers one can obtain the maximum possible refractive index of the medium while maintaining vanishing absorption [8, 9]. The maximum refractive index of an alkali vapor at a density of about $10^{15}$ atoms/cm$^3$ is $\approx 2$. The collisional broadening of the excited state prevents the refractive index to be increased further in an alkali vapor [9]. Demonstrating a refractive index of 2 in an alkali vapor with vanishing absorption may have significant practical implications. Since the wavelength of light is reduced inside the vapor, an optical microscope with two times better resolution may be constructed. Similarly, a better lithographic resolution may be obtained inside the medium. Furthermore, our scheme is general and may be applied to molecular species such as molecular $N_2$. In molecules, Raman transitions between vibrational and rotational states may be utilized, which may allow refractive index values approaching 10 to be obtained.

We also note the relation of our work to the growing field of negative index (left-handed) meta-materials [25]. Recently, there has been a number of theoretical suggestions that
achieve negative refractive index with low loss in the optical region of the spectrum in atomic systems [26, 27, 28]. We note that, by changing the order of gain and absorption resonances [such as in Fig. 3(c) and Fig. 3(d)], our scheme may also be used to obtain a reduced refractive index ($n < 1$). At large densities, this effect may be used to obtain a negative value of the dielectric permittivity, $\epsilon = 1 + \chi' < 0$, with vanishing absorption. While this is not sufficient to construct a negative index medium (since one also needs negative permeability, $\mu < 0$), it may be possible to combine our technique with a strong magnetic resonance in another specie and obtain a negative refractive index. A detailed analysis of this effect will be among our future investigations.

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