Research Article

A Multiview SAR Target Recognition Method Using Inner Correlation Analysis

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1. Introduction

With the continuous enhancement of synthetic aperture radar (SAR) data acquisition capabilities, it has become possible to acquire SAR images of the same target from multiple views, which provides more available information for correct target recognition [1]. Early SAR target recognition methods were mainly based on single-view SAR images, that is, to determine the target category in a single SAR image through effective feature extraction [2–18] and classification [19–32] with the support of training samples. There are relatively few research studies on target recognition methods based on multiview SAR images, whose basic idea can be divided into two categories [33–43]. One type considers that the SAR images from various views are relatively independent. So, the multiple views can be merged through the algorithm of parallel decision-making. In [33], researchers made use of SAR images from multiple views based on Bayesian theory-fused decision-making to obtain more reliable recognition results. Huan et al. first used support vector machine (SVM) to make independent decisions for each view and then proposed a decision fusion algorithm for different views based on the voting mechanism [38]. The other group believed that there were inherent connections between various views, which should be investigated. Zhang et al. first proposed a multiview SAR target recognition method based on joint sparse representation [39]. This method explored the internal associations between different views through joint sparse representation, thereby improving the accuracy of sparse representation of each view. Subsequently, many improved algorithms continued to appear under this framework, such as [40–42]. In theory, SAR images from different views of the same target must be related. However, due to the strong azimuth sensitivity of SAR images, the strength of this correlation is not stable enough. In other words, when the difference between the two views is small, the correlation between them is strong. Conversely, when the difference between the two views is large, the correlation between them is weak and not enough to reflect the internal correlation. Therefore, both independent inspection and joint representation are too arbitrary and cannot fully reflect the information contained in multiview SAR images.
Based on the above analysis, this paper fully examines the inner correlation in the multiview SAR images for target recognition. First, the correlation between two SAR images from different views is defined based on image correlation. On this basis, the correlation coefficient matrix between the multiview SAR images can be constructed to reflect the inherent correlation between different views. Then, the nonlinear correlation information entropy (NCIE) is used to calculate the correlations of a subset of the original multiview SAR images [44, 45]. The entropy represents the relevance of the selected viewing angle. Therefore, several multiview subsets with strong correlations can be obtained according to the resulted entropies. Finally, as a multitask processing algorithm, the joint sparse representation [39–41] is used for each set of SAR images to investigate the internal correlations of different views. It should be pointed out that there may only be one view in some collections, and the joint sparse representation will degenerate into the traditional sparse representation-based classification (SRC) at this time. For the decision value (reconstruction errors) output by each view set, the fusion errors are obtained in the form of linear weighting. And the target label of the multiview SAR image is determined according to the criterion of the smallest reconstruction error. In the experiment, the MSTAR dataset is used to comprehensively evaluate the proposed method. The result shows the effectiveness of the method in this paper.

\[
c = \max \left( \frac{\sum_{k,l} [I_1(k,l) - m_1] [I_2(k - \Delta k, l - \Delta l) - m_2]}{\sum_{k,l} [I_1(k,l) - m_1]^2[I_2(k - \Delta k, l - \Delta l) - m_2]^2}^{(1/2)} \right)
\]

where \( I_1 \) and \( I_2 \) represent two SAR images, \( m_1 \) and \( m_2 \) are their pixel averages, respectively, and \( \Delta k \) and \( \Delta l \) represent the sliding distance of the template image along the azimuth and distance directions. The correlation of SAR images is a prerequisite for multiview clustering in this study. In fact, there are many measures to evaluate the correlation of images. This study chooses a more classical image correlation coefficient, as shown in equation (1). The correlation coefficient examines the gray distribution difference between the two SAR images through pixel-level comparison. At the same time, the possible target registration errors are compensated by translation operations in two dimensions (range and azimuth). Therefore, the image correlation defined by equation (1) is more applicable in the evaluation of SAR image correlation in this study.

### 2.2. Clustering of Multiview SAR Images Based on NCIE

In order to effectively screen multiview SAR images reliably, this paper selects NCIE as the basic evaluation criterion for the internal correlation of different view sets [43, 44]. First, according to the similarity measure defined by equation (1), the correlation matrix between multiple views is constructed as follows:

\[
\mathbf{R} = \mathbf{E} + \bar{\mathbf{R}} = \begin{bmatrix}
1 & r_{12} & \cdots & r_{1N} \\
r_{21} & 1 & \cdots & r_{2N} \\
\vdots & \vdots & \ddots & \vdots \\
r_{N1} & r_{N2} & \cdots & 1
\end{bmatrix}
\]

where \( \mathbf{E} \) is the identity matrix and \( \bar{\mathbf{R}} \) represents the cross-correlation matrix between SAR images from \( N \) different views. According to the eigenvalues of \( \mathbf{R} \), the NCIE \( H_R \) is calculated as follows:

\[
H_R = 1 + \sum_{t=1}^{T} \frac{\lambda_t}{T} \log_{\lambda_t} \frac{\lambda_t}{T}
\]

According to equation (3), when all views have completely different distributions, the correlation coefficient matrix is a unit one and all eigenvalues are 1. At this time, the NCIE is the minimum value 0. When the similarity between the viewing angles is greater than 0, the eigenvalues of the correlation coefficient matrix are no longer equal. When different viewing angles have exactly the same distribution, the NCIE is the maximum value of 1. Therefore, according to the values of the NCIE, the inner correlations between different combinations of views can be obtained.

### 2. Clustering of Multiview SAR Images

Due to the SAR imaging mechanism, the target image is closely related to the relative view angle between itself and the radar sensor. This leads to SAR images with strong azimuth sensitivity. In actual multiview SAR target recognition, the views involved in decision-making come from different azimuth angles; whole difference and interval are unknown. At this time, if the azimuth angles of some view angles are quite different, their inherent correlation is weak. And the joint sparse representation of them directly may introduce wrong constraints. Conversely, if the azimuth angles of some viewing angles are relatively close, there is a strong correlation between them. If they are arbitrarily analyzed independently, effective information will be lost. Therefore, it is necessary to preanalyze their internal relations and then adopt some appropriate classification algorithms.

#### 2.1. Similarity Measure for SAR Images

Taking into account the independence and correlation between multiview SAR images, this study uses the idea of clustering to preprocess them. Specifically, the image correlation defined in equation (1) is used as the basic similarity measure for different views:
In this study, the NCIE is used to select the optimal view sets. For the candidate SAR images with different views, they are combined according to predetermined rules to obtain $P$ subset of different perspectives. Then, equation (3) is used to calculate the NCIE of each view set. Finally, according to the entropy sorting, the first $Q$ view sets are selected for the subsequent multiview recognition algorithm.

3. Proposed Recognition Algorithm

3.1. Multitask Sparse Representation. Inspired by the theory of compressive sensing, sparse representation theory was developed and widely used in the field of pattern recognition [39–41]. The basic idea of SRC is to use multiclass training samples to linearly represent test samples with unknown target label while constraining that the representation coefficients have strong sparseness. Assuming that the test sample is $y$, the training sample is $\{x_{1,1}, x_{1,2}, \cdots x_{1,n_1}, x_{2,1}, x_{2,2}, \cdots x_{2,n_2}, \cdots x_{M,1}, x_{M,2}, \cdots x_{M,n_M}\}$, where the subscripts $1$-$M$ correspond to different training classes and $n_k$ is the number of training samples of the $k$th class; the sparse representation can be described by the following equation:

$$y = \alpha_{1,1} x_{1,1} + \cdots \alpha_{m,n_m} x_{m,n_m} + \cdots \alpha_{M,n_M} x_{M,n_M} + \epsilon,$$  

(4)

where $\{\alpha_{1,1}, \cdots \alpha_{m,n_m}, \cdots \alpha_{M,n_M}\}$ is the sparse representation coefficient, that is, only a small number of the elements are nonzero.

The original SRC is mainly designed for a single signal or image. In fact, when there are multiple interrelated tasks for sparse representation at the same time, the correlation between them can be used to improve the accuracy of the representation. As a result, the joint sparse representation was proposed and applied. Let $K$ related tasks be $y = [y^{(1)}, y^{(2)}, \cdots, y^{(K)}]$, their joint sparse representation problem is as follows:

$$y^{(k)} = D^{(k)} \alpha^{(k)} + \epsilon^{(k)}, \quad (k = 1, 2, \cdots, K),$$  

(5)

where $y^{(k)}$, $D^{(k)}$, and $\alpha^{(k)}$ represent the test sample, training sample dictionary, and representation coefficient under the sparse representation task, respectively. In order to jointly solve the sparse representation coefficient vectors of multiple tasks, the optimization objective function shown in equation (6) can be used:

$$\min_{\beta} \left\{ g(\beta) = \sum_{k=1}^{K} \| y^{(k)} - D^{(k)} \alpha^{(k)} \| \right\},$$  

(6)

where $\beta = [\alpha^{(1)}, \alpha^{(1)} \cdots \alpha^{(K)}]$ is a matrix containing the sparse coefficients.

Equation (6) ignores the correlation between different tasks in the optimization solution. In order to further improve the accuracy of the joint sparse representation, the sparse representation coefficient matrix can be appropriately constrained to make use of the associations seen in each task, as shown below:

$$\min_{\beta} \left\{ g(\beta) + \lambda \| \beta \|_{2,1}, \right\}$$  

(7)

where $\| \cdot \|_{2,1}$ denotes the $\ell_1/\ell_2$ norm. By adding this regular term, it is possible to constrain the sparse representations of different tasks to have similar sparse distribution characteristics (that is, the distribution law of nonzero coefficients), so as to explore the inherent relationship between them. To solve this problem, the algorithms in [39–41] can be used to solve the sparse representation coefficient matrix. Finally, the reconstruction error of each training class for multitask test samples can be calculated as follows:

$$f(i) = \sum_{k=1}^{K} \| y^{(k)} - D^{(k)} \alpha^{(k)} \|,$$  

(8)

where $D^{(k)}$ and $\alpha^{(k)}$ represent the dictionary and sparse representation coefficients corresponding to the class under the $k$th task, respectively.

3.2. Recognition Procedure. In this study, a new classification strategy is designed for the target recognition problem of multiview SAR images. Through multiview clustering, the independence and correlation of multiview SAR images are effectively investigated. Then, the joint sparse representation is used to independently analyze each set of views with inherent correlation to obtain the reconstruction errors. The output reconstruction error of each view set is denoted as $f_i(i) (i = 1, 2, \cdots, P)$. Then, the linear weighting is used to fuse them as follows:

$$e(i) = \omega_1 f_1(i) + \omega_2 f_2(i) + \cdots + \omega_p f_p(i),$$  

(9)

where $\omega_i (i = 1, 2, \cdots, P)$ is the weight coefficient. In this study, the weight is determined according to the number of SAR images in each view set as $\omega_i = (p_i/P)$, where $p_i$ is the number of images in the $i$th view set. Finally, the target label is determined according to the weighted reconstruction error of each training class.

Figure 1 shows the basic process of the method in this paper, including multiview clustering, multiview joint sparse representation, and linear weighted fusion of the results of each view set. The final recognition performance can be improved by examining the independence and correlation of multiview SAR images. In the specific implementation, in order to reduce the dimensionality of the SAR images, a random projection algorithm is used to transform it into a 520-dimensional feature vector according to [39]. It is worth noting that when some clustering results contain only one SAR image, the joint sparse representation degenerates to the traditional SRC, which does not affect the implementation of the proposed method.

4. Experiments

4.1. MSTAR Dataset. This study uses the SAR images of ten types of MSTAR targets (the optical images are shown in Figure 2) to test the proposed method. All the SAR images have the same resolution of $0.3 \times 0.3$. A typical experimental setup is listed in Table 1. Among them, the
Trainingsamples are collected from a 17° depression angle, and the test samples are collected from a 15° depression angle. In addition, by some simulation algorithms such as noise addition and occlusions, more experimental conditions can be generated to further evaluate the proposed method.

For comparison, this paper sets up several types of reference methods, including both the traditional single-view ones and the recently published multiview SAR target recognition ones. The single-view SAR target recognition method based on the SRC in [23] and the convolutional neural network (CNN)-based method in [28] are selected as the references. In the SRC method, the random projection is used to reduce the original SAR image to a 520-dimensional feature vector, which is consistent with the method in this paper. The CNN method is directly based on the original gray value of the SAR image for training and classification. The multiview methods in [38, 39] are selected for comparison, and they are recorded as “parallel multiview” and “joint multiview” methods, respectively. The parallel multiview method considers that each perspective is independent of each other, and makes decisions for each perspective and finally merges it. The joint multiview method is considered that multiview SAR images are inherently related, so they are unified and jointly expressed, and the target label is determined according to the sum of the final reconstruction errors.

4.2. Results and Analysis

4.2.1. Preliminary Validation. First, the proposed method is tested under the conditions of a fixed number of views. When the number of views is set to 3 and the azimuth angle interval of different viewing angles is 2°, the recognition results of the proposed method on the 10 types of targets under the conditions of Table 1 can be expressed as the

Table 1: A typical experimental setup based on the MSTAR dataset.

| Class     | Training (17°) | Test (15°) |
|-----------|----------------|------------|
| BMP2      | 233            | 195        |
| BTR70     | 233            | 196        |
| T72       | 232            | 196        |
| T62       | 299            | 273        |
| BRDM2     | 298            | 274        |
| BTR60     | 256            | 195        |
| ZSU23/4   | 299            | 274        |
| D7        | 299            | 274        |
| ZIL131    | 299            | 274        |
| 2S1       | 299            | 274        |

training samples are collected from a 17° depression angle, and the test samples are collected from a 15° depression angle. In addition, by some simulation algorithms such as noise addition and occlusions, more experimental conditions can be generated to further evaluate the proposed method.

Figure 1: Procedure of target recognition based on clustering and joint representation of multiview SAR images.

Figure 2: Images of the 10 targets for experiments. (a) BMP2 (b) BTR70 (c) T72 (d) BTR60 (e) 2S1, (f) BRDM2 (g) D7 (h) T62 (i) ZIL131 (j) ZSU23/4.
confusion matrix shown in Figure 3. It can be seen that the correct recognition rates of various targets (corresponding to the diagonal elements in the figure) is above 98.5%, and the average recognition rate is 99.42%. Table 2 shows the average recognition rates of various reference methods under current conditions. In general, since the target information provided by multiview SAR images is more comprehensive, the recognition rates of the three types of multiview methods maintain a relatively high level and outperform the single-view ones. CNN can obtain strong classification ability when the training samples are sufficient, so it has also achieved high recognition performance. The comparison results show that the method in this paper is the most effective for 10 types of target recognition problems.

4.2.2. Performance at Different Numbers of Views. The number of views is an important parameter in the multiview SAR target recognition method. For this reason, this experiment tests the recognition performance of the proposed method under different view angles. When the azimuth interval of different viewing angles is set to 2°, the average recognition rates of the three types of multiview methods varies with the viewing angle, as shown in Figure 4. The recognition performance of the method in this paper is increasing with the increase of the number of viewing angles. For the parallel multiview method, the recognition rate is also increasing, but the overall level remains relatively low. In the joint multiview method, when the number of views is less than 4, the recognition rate keeps increasing. However, when the number of viewing angles is large, the recognition rate decreases slightly. This is mainly because, at this time, a part of the viewing angles has relatively weak internal correlation due to the large azimuth angle difference, which

Table 2: Average recognition rates achieved by different methods.

| Method type         | Average recognition rate (%) |
|---------------------|------------------------------|
| Proposed            | 99.42                        |
| SRC                 | 97.68                        |
| CNN                 | 99.06                        |
| Parallel multiview  | 99.12                        |
| Joint multiview     | 99.30                        |

Figure 3: Results of 10-class recognition achieved by the proposed method.

Figure 4: The recognition performance of the multiview methods at different view numbers.
leads to a decrease in the accuracy of the joint sparse representation.

4.2.3. Noise Corruption. The recognition performance of the proposed method under noise interference conditions is investigated by adding different degrees of Gaussian white noise to the test samples in Table 1. The specific noise adding process can be found in [17]. Figure 5 shows the recognition performance of various methods under noise interference conditions. Among them, the number of viewing angles of the multiview method is set to 3, and the azimuth angle interval is 2°. The method in this paper maintains the highest average recognition rate under each signal-to-noise ratio (SNR), verifying its robustness to noise corruption. Compared with single-view methods, the performance of the three types of multiview methods is better, mainly due to the fact that multiview SAR images can provide more effective information for classification. The method in this paper further improves the robustness of the recognition method against noise interference by carefully examining the independence and correlation of multiview SAR images.

5. Conclusion

This paper proposes a multiview SAR target recognition method. For the multiple views involved in decision-making, their inner correlations are first analyzed based on image correlation and NCIE. Several view sets with strong internal correlations are obtained. Then, the joint sparse representation is used to investigate the internal association of the SAR images in each view set. Finally, a more robust decision variable is obtained through linear weighted fusion, so as to determine the target label more accurately. The experimental results based on the MSTAR dataset show that the method in this paper can achieve good recognition performance under a variety of experimental conditions, verifying its effectiveness.

Data Availability

The dataset used to support the findings of the study are obtained from the corresponding author upon request.

Conflicts of Interest

The authors declare no conflicts of interest.

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References

[1] K. El-Darymli, E. W. Gill, D. Power, and C. Moloney, “Automatic target recognition in synthetic aperture radar imagery: a state-of-the-art review,” IEEE Access, vol. 4, pp. 6014–6058, 2016.
[2] M. Ammoon and G. a. Rezai-rad, “Automatic target recognition of synthetic aperture radar (SAR) images based on optimal selection of Zernike moments features,” IET Computer Vision, vol. 8, no. 2, pp. 77–85, 2014.
[3] B. Ding, G. Wen, C. Ma, and X. Yang, “Target recognition in synthetic aperture radar images using binary morphological operations,” Journal of Applied Remote Sensing, vol. 10, no. 4, Article ID 046006, 2016.
[4] C. Shan, B. Huang, and M. Li, “Binary morphological filtering of dominant scattering area residues for SAR target recognition,” Computational Intelligence and Neuroscience, vol. 2018, Article ID 9680465, 2018.
[5] L. Jin, J. Chen, and X. Peng, “Synthetic aperture radar target classification via joint sparse representation of multi-level dominant scattering images,” Optik, vol. 186, pp. 110–119, 2019.
[6] J. Tan, X. Fan, S. Wang et al., “Target recognition of SAR images by partially matching of target outlines,” Journal of Electromagnetic Waves and Applications, vol. 33, no. 7, pp. 865–881, 2019.
[7] S. Papson and R. M. Narayanan, “Classification via the shadow region in SAR imagery,” IEEE Transactions on Aerospace and Electronic Systems, vol. 48, no. 2, pp. 969–980, 2012.
[8] A. K. Mishra, “Validation of PCA and LDA for SAR ATR,” in Proceedings of the IEEE TENCON, pp. 1–6, Osaka, Japan, November 2008.
[9] Z. Cui, Z. Cao, J. Yang, J. Feng, and H. Ren, “Target recognition in synthetic aperture radar images via non-negative matrix factorisation,” IET Radar, Sonar & Navigation, vol. 9, no. 9, pp. 1376–1385, 2015.
[10] W. Xiong, L. Cao, and Z. Hao, “Combining wavelet invariant moments and relevance vector machine for SAR target recognition,” IET International Radar Conference, vol. 4, pp. 1–4, 2009.
[11] G. Dong, G. Kuang, N. Wang, L. Zhao, and J. Lu, “SAR target recognition via joint sparse representation of monogenic signal,” IEEE Journal of Selected Topics in Applied Earth
Observations and Remote Sensing, vol. 8, no. 7, pp. 3316–3328, 2015.
[12] Y. Zhou, Y. Chen, and R. Gao, "SAR target recognition via joint sparse representation of monogenic components with 2D canonical correlation analysis," IEEE Access, vol. 7, pp. 25815–25826, 2019.
[13] M. Chang, X. You, and Z. Cao, "Bidimensional empirical mode decomposition for SAR image feature extraction with application to target recognition," IEEE Access, vol. 7, pp. 135720–135731, 2019.
[14] M. Yu, G. Dong, H. Fan, and G. Kuang, "SAR target recognition via local sparse representation of multi-manifold regularized low-rank approximation," Remote Sensing, vol. 10, no. 2, p. 211, 2018.
[15] Y. Huang, J. Peia, J. Yanga, B. Wang, and X. Liu, "Neighborhood geometric center scaling embedding for SAR ATR," IEEE Transactions on Aerospace and Electronic Systems, vol. 50, no. 1, pp. 180–192, 2014.
[16] L. C. Potter and R. L. Moses, "Attributed scattering centers for SAR ATR," IEEE Transactions on Image Processing, vol. 6, no. 1, pp. 79–91, 1997.
[17] B. Ding, G. Wen, J. Zhong, C. Ma, and X. Yang, "A robust similarity measure for attributed scattering center sets with application to SAR ATR," Neurocomputing, vol. 219, pp. 130–143, 2017.
[18] B. Ding, G. Wen, X. Huang, C. Ma, and X. Yang, "Target recognition in synthetic aperture radar images via matching of attributed scattering centers," IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing, vol. 10, no. 7, pp. 3334–3347, 2017.
[19] Q. Zhao and J. C. Principe, "Support vector machines for SAR automatic target recognition," IEEE Transactions on Aerospace and Electronic Systems, vol. 37, no. 2, pp. 643–654, 2001.
[20] M. E. Demirhan and O. Salor, "Classification of targets in SAR images using SVM and k-NN techniques," in Proceedings of the 2016 24th Signal Processing and Communication Application Conference (SIU), pp. 1581–1584, Zonguldak, Turkey, May 2016.
[21] H. Liu and S. Li, "Decision fusion of sparse representation and support vector machine for SAR image target recognition," Neurocomputing, vol. 113, pp. 97–104, 2013.
[22] J. J. Thiaigaraianm, K. N. Ramamurthy, P. Knee, A. Spanias, and V. Berisha, "Sparse representations for automatic target classification in SAR images," in Proceedings of the 4th International Symposium on Communication Systems, pp. 1–4, Roma, Italy, May 2010.
[23] H. Song, K. Ji, and Y. Zhang, "Sparse representation-based SAR image target classification on the 10-class MSTAR data set," Applied Sciences, vol. 6, no. 26, 2016.
[24] B. Ding and G. Wen, "Sparsity constraint nearest subspace classifier for target recognition of SAR images," Journal of Visual Communication and Image Representation, vol. 52, pp. 170–176, 2018.
[25] W. Li, J. Yang, and Y. Ma, "Target recognition of synthetic aperture radar images based on two-phase sparse representation," Journal of Sensors, vol. 2020, Article ID 2032643, 2020.
[26] L. Yu, L. Wang, and Y. Xu, "Combination of joint representation and adaptive weighting for multiple features with application to sar target recognition," Scientific Programming, vol. 2021, Article ID 9063419, 2021.
[27] X. X. Zhu, D. Tuia, L. Mou et al., "Deep learning in remote sensing: a comprehensive review and list of resources," IEEE Geoscience and Remote Sensing Magazine, vol. 5, no. 4, pp. 8–36, 2017.