TESTING FOR A LARGE LOCAL VOID BY INVESTIGATING THE NEAR-INFRARED GALAXY LUMINOSITY FUNCTION

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ABSTRACT

Recent cosmological modeling efforts have shown that a local underdensity on scales of a few hundred Mpc (out to \( \sim 400 \) Mpc) could produce the apparent acceleration of the expansion of the universe observed via Type Ia supernovae. Several studies of galaxy counts in the near-infrared (NIR) have found that the local universe appears underdense by \( \sim 25\%–50\% \) compared with regions a few hundred Mpc distant. Galaxy counts at low redshifts sample primarily \( L \sim L^* \) galaxies. Thus, if the local universe is underdense, then the normalization of the NIR galaxy luminosity function (LF) at \( z > 0.1 \) should be higher than that measured for \( z < 0.1 \). Here we present a highly complete (>90%) spectroscopic sample of 1436 galaxies selected in the \( H \) band (1.6 \( \mu m \)) to study the normalization of the NIR LF at \( 0.1 < z < 0.3 \) and address the question of whether or not we reside in a large local underdensity. Our survey sample consists of all galaxies brighter than 18th magnitude in the \( H \) band drawn from six widely separated fields at high Galactic latitudes, which cover a total of \( \sim 2 \) deg\(^2\) on the sky. We find that for the combination of our six fields, the product \( \phi^*L^* \) at \( 0.1 < z < 0.3 \) is \( \sim 30\% \) higher than that measured at lower redshifts. While our statistical errors in this measurement are on the \( \sim 10\% \) level, we find the systematics due to cosmic variance may be larger still. We investigate the effects of cosmic variance on our measurement using the COSMOS cone mock catalogs from the Millennium Simulation and recent empirical estimates of cosmic variance. We find that our survey is subject to systematic uncertainties due to cosmic variance at the 15% level (1\( \sigma \)), representing an improvement by a factor of \( \sim 2 \) over previous studies in this redshift range. We conclude that observations cannot yet rule out the possibility that the local universe is underdense at \( z < 0.1 \). The fields studied in this work have a large amount of publicly available ancillary data and we make available the images and catalogs used here.

Key words: cosmology: observations – galaxies: fundamental parameters

Online-only material: color figures

1. INTRODUCTION

The size of large-scale structures in the local universe (e.g., sheets, voids, and superclusters of galaxies), and our location among them, is of critical importance to the interpretation of observational results. Cosmic variance due to large-scale structure can lead to systematic variations in observational data. Such systematics can dominate over other sources of error if a volume sufficient to average over cosmic variance has not been sampled. However, it remains unclear just what the upper limit on the size of large-scale structure is, and hence what volume constitutes a representative sample of the universe. If the typical size of local large-scale structure is much greater than 100 Mpc, then local measurements of the Hubble constant, and other cosmological observables, could still harbor large systematic errors. We make our images and catalogs publicly available at http://www.asiaa.sinica.edu.tw/urkeenan.

Cold dark matter simulations that include a cosmological constant (\( \Lambda \)CDM models), such as the Millennium Run (Springel et al. 2005), predict that the largest dark matter structures in the universe should be \( \sim 100 \) Mpc in extent. Observed luminous matter large-scale structures, most notably the >400 Mpc Sloan Great Wall (Gott et al. 2005), demonstrate the existence of structure on larger scales than simulations predict (assuming luminous matter traces dark matter). It has also been shown that voids on scales similar to that of the Sloan Great Wall may explain the “cold spots” in the cosmic microwave background (Inoue & Silk 2006). It is not yet clear whether such structures represent extreme nonlinearities in the matter distribution of the universe, or if inhomogeneities on several hundred Mpc scales are typical.

Cosmologists have proposed the so-called void models as alternatives to \( \Lambda \)CDM that invoke a large local underdensity to explain the apparent acceleration of the expansion of the universe (Alnes et al. 2006; Chung & Romano 2006; Enqvist & Mattsson 2007; García-Bellido & Haugbølle 2008a, 2009; Alexander et al. 2009; February et al. 2010; Célérier et al. 2010; Biswas et al. 2010; Marra & Pålkkönen 2010; Clarkson & Maartens 2010; Bolejko & Sussman 2011). The scale of the voids proposed in these models ranges from a few hundred Mpc to several Gpc in radius. The basic premise of void models is that if we, as observers, live near the center of a large underdensity, then we would witness a local expansion of the universe that is faster than the global expansion, simply due to the void being evacuated toward higher-density surroundings via gravity. This would provide a locally measured Hubble constant that is higher than the global value and look observationally like an accelerating expansion.

In their current form, void models with \( \Lambda = 0 \) appear not to be viable alternatives to \( \Lambda \)CDM, as they have trouble fitting the entire range of cosmological observables (García-Bellido & Haugbølle 2008b; Zibin et al. 2008; Moss et al. 2011; Zhang & Stebbins 2011; Riess et al. 2011). However, the exploration of this class of cosmological models, and other inhomogeneous
models, has highlighted the need for a more comprehensive understanding of large-scale structure in the universe and our location within it (e.g., Marra & Notari 2011; Bolejko et al. 2011; Bull & Clifton 2012). In particular, the so-called minimal void scenarios (e.g., Alexander et al. 2009; Bolejko & Sussman 2011) have shown that very simple models that place the observer near the center of a void that is \( \sim 250 \, h^{-1} \, \text{Mpc} \) in radius (to \( z \sim 0.1 \)) and \( \sim 50\% \) underdense compared with its surroundings are sufficient to explain the apparent acceleration observed via Type Ia supernovae. While these models are simplistic, they point out that our location within local structure may have profound implications for our measurement of cosmological observables.

The existence of a large local void would be consistent with studies of near-infrared (NIR) galaxy counts that have found the local space density of galaxies may be low by 25\%–50\% compared with the density at distances of \( \sim 300 \, h^{-1} \, \text{Mpc} \) or \( z \sim 0.1 \) (Keenan et al. 2010b; Busswell et al. 2004; Frith et al. 2003, 2005; Huang et al. 1997). Galaxy counts in the NIR at low redshifts are primarily sampling \( L \sim L^* \) or brighter galaxies (Barro et al. 2009). Thus, if the universe at \( z < 0.1 \) is underdense, the normalization of the NIR luminosity function (LF) at \( z > 0.1 \) should be higher than locally measured values. In this paper, we explore the normalization of the NIR LF as a function of redshift to test for the existence of a large local underdensity.

At \( z < 0.1 \), the NIR LF has been studied using samples selected from large NIR surveys, such as the Two Micron All Sky Survey (2MASS; Skrutskie et al. 2006) and the UKIRT Infrared Deep Sky Survey (UKIDSS; Lawrence et al. 2007), combined with spectroscopy from redshift surveys, such as the CfA2 redshift survey (Geller & Huchra 1989; Huchra et al. 1992), the Two-degree Field Galaxy Redshift Survey (2dFGRS; Colless et al. 2001), and the Sloan Digital Sky Survey (SDSS; York et al. 2000).

Using these data, the \( \langle z \rangle \sim 0.05 \) NIR LF has been relatively well established (Cole et al. 2001; Kochanek et al. 2001; Jones et al. 2006). Studies at slightly higher median redshifts (0.07 < \( z < 0.1 \)) tend to arrive at a normalization that is a factor of \( \sim 1.5 \) higher, though they state general consistency with lower redshift measurements when possible systematics due to differences in methodology, etc. (Bell et al. 2003; Eke et al. 2005; Smith et al. 2009; Hill et al. 2010). Taken together, however, the aforementioned studies appear to point to the possibility of an increasing LF normalization from \( z \sim 0.05 \) to \( z \sim 0.1 \).

Ideally, one would like to study the total luminosity density (and hence stellar mass density) as a function of distance rather than just simply the normalization of the LF. However, any apparent magnitude-limited survey at low redshifts is limited on the bright end of the LF by poor counting statistics and on the faint end by the relatively small(er) volume over which faint galaxies may be sampled. These two effects, along with differences in methodology, combine to yield the result that the overall shape of the NIR LF can be quite different from one study to the next. These differences in LF shape can lead to substantial differences in integrated luminosity density.

The peak contribution of the LF to the total luminosity density occurs at \( L \sim L^* \), where all studies feature the best statistics. The Schechter (1976) function parameters for the normalization (\( \phi^* \)) and characteristic luminosity (\( L^* \)) are correlated. Thus, in this study we focus on a comparison between our study and those from the literature of the product of the normalization and characteristic luminosity (\( \phi^* L^* \)), which amounts to a comparison of the peak of the luminosity density distribution across studies.

In this paper, we probe the NIR LF just beyond the local volume at redshifts of 0.1 < \( z < 0.3 \). To study the NIR LF at these relatively low redshifts, high spectroscopic completeness is essential to overcome possible biases and to deal with the fact that the errors in the photometric redshifts are of the order of the redshifts themselves (i.e., \( \sigma_z / z \sim 1 \)). Our spectroscopic survey of H-band-selected galaxies (\( H_{AB} < 18 \)) is >90\% complete over six widely separated fields covering a total of 2 deg\(^2\) on the sky. Rest-frame H-band light is a good tracer of stellar mass and hence a galaxy’s H-band luminosity (in solar units) is approximately equal to its stellar mass (in solar units; de Jong 1996; Bell & de Jong 2001; Bell et al. 2003; Kirby et al. 2008). At low redshifts, \( \lambda_{\text{observed}} \approx \lambda_{\text{rest}} \), and, in the NIR, K-corrections are small and nearly independent of galaxy type (Mannucci et al. 2001), so this is effectively a mass-selected sample.

Our survey is unique among extragalactic redshift surveys because of its relative depth, width, and spectroscopic completeness. Deep redshift surveys, such as the Cosmic Evolution Survey (COSMOS/ZCOSMOS, Scoville et al. 2007b; Lilly et al. 2009), the All-wavelength Extended Groth strip International Survey plus the Deep Evolutionary Exploratory Survey 2 (AEGIS + DEEP2, Davis et al. 2007), and the VIMOS VLT Deep Survey (VVDS; Le Fèvre et al. 2005) all feature high-quality NIR photometry and \( \sim 10,000 \) publicly available redshifts each. However, the spectroscopic completeness at relatively bright NIR magnitudes (\( H_{AB} < 18 \)) is less than 40\% in all cases. The Galaxy And Mass Assembly survey (GAMA; Driver et al. 2011) will feature high completeness to \( K \sim 18 \), although the current public data release is only complete to \( K \sim 16 \).

The structure of this paper is as follows. We present our observations, data reduction, and redshift determination methods in Section 2. We discuss our methods of spectral energy distribution (SED) fitting to obtain photometric redshifts for targets lacking spectroscopy in Section 3. We present our results regarding the observed NIR LFs in Section 4. We analyze the effects of cosmic variance on our study and the last decade of studies of the NIR LF in the literature in Section 5. We summarize in Section 6. Unless otherwise noted, all magnitudes given in this paper are in the AB magnitude system (\( m_{AB} = 23.9 - 2.5 \log_{10} f_\lambda \) with \( f_\lambda \) in units of \( \mu \text{Jy} \)). We assume a cosmology of \( \Omega_M = 0.27 \), \( \Omega_{\Lambda} = 0.73 \), and \( h = 0.7 \) in our conversion of redshifts to distances.

### 2. OBSERVATIONS AND DATA REDUCTION

Our primary photometry covers six fields in the \( J, H, \) and \( K \) bands. In Table 1, we show the location of our observed fields in right ascension and declination, as well as Galactic and supergalactic coordinates. Also shown in Table 1 are the area on the sky, number of target galaxies, and spectroscopic completeness for each field.

We made all the \( H \)- and \( J \)-band observations (except the CDF-N \( J \)-band) with the Ultra-Low Background Camera (ULBCam) on the UH2.2 m telescope. We observed the Chandra Deep Field North (CDF-N) in the \( K_s \) band with the Wide-field Infrared Camera (WIRCam) at the Canada–France–Hawaii Telescope 3.6 m (CFHT). CDF-N \( J \)-band observations with WIRCam were obtained by a group led by Lihwai Lin in 2006. Our group reduced these public data in 2008. We observed five of our six fields in the \( K \) band with WFCam on UKIRT.
We presented the observations, data reduction, star–galaxy separation, and bright galaxy counts for our deep wide-field NIR imaging campaign in Keenan et al. (2010b). In that paper, we used the bright NIR galaxy counts from our survey in combination with other data from the literature to explore local large-scale structure via the slope of the galaxy counts curve as a function of position on the sky. In Keenan et al. (2010a), we integrated galaxy counts from our NIR survey in combination with deeper data from the Multi Object InfraRed Camera and Spectrograph (MOIRCS) instrument on the Subaru Telescope, and other studies from the literature, to obtain the best current estimate of the total light from galaxies in the NIR.

The portion of the survey used for this work includes only areas where all three bands have uniform coverage and consists of approximately 2 deg² reaching a 5σ limiting magnitude of JHK ∼ 22–23 over ∼ 1.8 deg² with another ∼ 0.2 deg² to JHK ∼ 24. Thus, the NIR photometry used for the present work has very high signal to noise.

Before performing photometry on galaxies, we calibrated our NIR images to 2MASS fluxes using relatively bright point sources in the magnitude range 14 < JHK < 16, where 2MASS reports better than 10σ signal to noise and our data are well below saturation levels. We found our final calibrated images to be quite flat and free from systematic variations in flux as a function of position. We used the SExtractor (Bertin & Arnouts 1996). For a detailed description of all processes in the Megapipe reduction, please refer to the Web site http://cadcwww.dao.nrc.ca/megapipe. The MegaCam pipeline Web site (Megapipe6). The MegaCam u, g, r, and i bands (there were no z-band observations for A370). We downloaded the catalogs from the MegaCam image stacking pipeline Web site (Megapipe6). The MegaCam u, g, r, and i filters are quite similar to those of the SDSS,7 and small magnitude offsets provided on the Megapipe Web site bring the data into accordance with SDSS magnitudes.

Catalogs generated through Megapipe are processed in the following way: Raw images are reduced or “detrended” through the Elixir8 system, which includes treatment for dark and bias subtraction, flat fielding, defringing, and basic astrometric and photometric calibration. Elixir-processed images are retrieved and checked for quality before stacking. More refined processing for astrometric and photometric calibrations are performed and then the images are co-added. Catalogs are generated through the application of the source extraction software SExtractor (Bertin & Arnouts 1996). For a detailed description of all processes in the Megapipe reduction, please refer to the Web site http://cadcwww.dao.nrc.ca/megapipe.

Three of our fields (CLANS, CLASXS, and CDF-N) are covered by the SDSS, which allows us to use uniform photometry for fitting SEDs. In addition to the fields that were presented in Keenan et al. (2010b; CLANS, CLASXS, CDF-N, A370, and SSA13), we added the blank field “SSA17.” The NIR data reduction and photometry methods for the SSA17 field were identical to those described in Keenan et al. (2010b) for the other fields, except SSA17 does not include K-band photometry.

In the case of the A370 field, we use publicly available optical photometry from the CFHT MegaCam in the u, g, r, and i bands (there were no z-band observations for A370). We downloaded the catalogs from the MegaCam image stacking pipeline Web site (Megapipe6). The MegaCam u, g, r, and i filters are quite similar to those of the SDSS,7 and small magnitude offsets provided on the Megapipe Web site bring the data into accordance with SDSS magnitudes.

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### Table 1

| Field       | CDF-N | CLANS | CLASXS | SSA13 | SSA17 | A370 |
|-------------|-------|-------|--------|-------|-------|------|
| R.A. (hh:mm:ss) | 12:36:55 | 10:46:54 | 10:34:58 | 13:12:16 | 17:06:31 | 02:39:53 |
| Decl. (dd:mm:ss) | 62:14:19 | 59:08:26 | 57:52:22 | 42:41:24 | 43:55:44 | −01:34:37 |
| Galactic l (deg) | 125.9 | 148.2 | 151.5 | 109.1 | 68.9 | 173 |
| Galactic b (deg) | 54.8 | 51.4 | 51.0 | 73.8 | 42.0 | −53.5 |
| Supergalactic l (deg) | 54.7 | 52.2 | 52.3 | 75.3 | 65.1 | 302.3 |
| Supergalactic b (deg) | 11.7 | −1.8 | −3.9 | 13.6 | 49.5 | −25.7 |
| Area (deg²) | 0.2 | 0.5 | 0.5 | 0.2 | 0.2 | 0.4 |
| Spectroscopic Redshifts | 92 | 297 | 278 | 121 | 161 | 367 |
| Total Targets (H < 18) | 100 | 313 | 298 | 124 | 188 | 413 |

(1) http://cadcwww.dao.nrc.ca/megapipe
(7) http://cadcwww.dao.nrc.ca/megapipe/docs/filters.html
(8) http://www.cfht.hawaii.edu/Instruments/Elixir

2.1. Fields Observed

Our first two fields are centered on the Chandra Large Area Synoptic X-ray Survey (CLASXS; Yang et al. 2004; Steffen et al. 2004) and the Chandra Lockman Area North Survey (CLANS; Trouille et al. 2008, 2009). Each of these fields cover ∼ 0.5 deg² in JHK. These fields are located in the Lockman Hole region of low Galactic H I column density (Lockman et al. 1986). Our third field covers a ∼ 0.2 deg² area centered on the CDF-N (Brandt et al. 2001; Alexander et al. 2003). The CDF-N contains the Great Observatories Origins Deep Survey North (GOODS-N; 145 arcmin²) HST Advanced Camera for Surveys observation; Giavalisco et al. 2004). Our fourth field is the Abell 370 (A370) cluster and surrounding area (∼ 0.4 deg²). A370 is a cluster of richness 0 at a redshift of z = 0.37. Our fifth and sixth fields are ∼ 0.2 deg² each centered on the “Small-Survey-Area 13” (SSA13) and “Small-Survey-Area 17” (SSA17) from the Hawaii Deep Fields described in Lilly et al. (1991).
we use the Spitzer Wide-area InfraRed Extragalactic Survey catalogs (SWIRE; Lonsdale et al. 2003) to supplement the photometry for 516 of our target galaxies. In the CDF-N, we use the IRAC catalogs of Wang et al. (2010) to supplement the photometry for an additional 33 targets. As a result, almost 40% of our target galaxies have high-quality photometry in the mid-infrared.

2.3. Spectroscopic Observations and Reductions

We observed our target galaxies between 2006 and 2010 with the Hydra fiber spectrograph instrument (Barden & Armandroff 1995) on the Wisconsin–Indiana–Yale–NOAO (WIYN) telescope at Kitt Peak in Arizona. Hydra is a multi-fiber spectrograph with ~90 functioning fibers in the configuration we used. The field of view of this instrument is 1 deg in diameter on the sky and fibers may be placed a minimum of 37" apart. We configured the fibers using the whydra configuration code, which allows the user to define a minimum number of sky positions and guide stars required and allows for targets to be weighted by priority. We also used the hydrasim simulator code to check that the output of whydra was compatible with the software at the telescope. The hydra “red” fibers are 2" in diameter, which were ideally suited to getting the majority of light from our target galaxies onto the spectrograph with minimum contamination from the sky and neighboring sources.

For this survey we selected galaxies from our H-band photometry (H < 18). We masked areas of our images near bright objects (R magnitude < 14.5), as described in Keenan et al. (2010b), to avoid targets that were blended with bright neighbors. This selection yielded 1436 target galaxies in the range 14.5 < H < 18.

We configured the spectrograph using the “red” fiber bundle and the 316@7.0 grating at first order with the GG-420 filter to provide a spectral window of ~4000–9500 Å with a pixel scale of 2.6 Å pixel⁻¹. Toward the edges of our spectral window the spectra were often dominated by noise due to the waning sensitivity of the spectrograph on the blue end and the spectrum becoming sky dominated in the red. As a result, the useable spectral window was ~4500–9000 Å. We obtained the majority of our target spectra since 2008 when the bench spectrograph at WIYN was upgraded (Bershady et al. 2008). The improved sensitivity of the upgraded bench spectrograph allowed us to determine redshifts for ~90%–100% of target galaxies in a two-hour exposure given ideal observing conditions.

Our exposures were typically 20 minutes each, and we would stay on target for 1–3 hr total, depending on the observing conditions and the targets observed. For calibration we took dark frames, bias (zero exposure time) frames, dome flats, and CuAr comparison lamp exposures. We employed the IRAF task dohydra⁹ in the reduction of our spectra. This task is specifically designed for reduction of data from the Hydra spectrograph and includes steps for dark and bias subtraction, flat fielding, dispersion calibration, and sky subtraction.

2.4. Redshift Determination

We used the IRAF task xcsao within the rvsao package (Kurtz & Mink 1998) to determine redshifts for our observed spectra. The xcsao task is an interactive tool that allows the user to determine redshifts by cross-correlating a spectrum against template spectra using methods described in Tonry & Davis (1979). This task allows the user to manually mask portions of the spectrum and cycle through a variety of candidate fits to find the best match. We manually determined a redshift for all of the galaxies in our spectroscopic sample using xcsao in this manner.

At the relatively low redshifts of our sample galaxies, the commonly identifiable absorption features in our spectra were Ca ii H (3969 Å) and K (3934 Å), the 4000 Å break, the Fe G-band feature (~4100 Å), Hγ (4342 Å), Hβ (4865 Å), and the Na D lines (5890/5896 Å). If emission lines were present, our spectra typically captured the He α (6563 Å) and [N ii] (6548/6584 Å) complex along with the [S ii] doublet (6719/6730 Å) and/or the [O iii] (3727 Å), [O iii] (4961/5007 Å), and Hβ (4865 Å) emission lines.

For ~50 galaxies we targeted objects that already had a cataloged redshift in the SDSS archive. We find 100% agreement with the SDSS redshifts to within an rms error of 0.0005. We supplement our catalogs with an additional 32 redshifts from the SDSS for other targets in our fields. We also supplement our catalogs with 129 redshifts for objects in our fields that were either previously published in the literature or obtained from other spectroscopic campaigns within our research group.

For the CDF-N field, many of these supplementary redshifts are cataloged in Barger et al. (2008) and references therein. In the CLANS and CLASXS fields, many of the supplementary redshifts are cataloged in Trouille et al. (2008, 2009). Many redshifts in the SSA13 field are cataloged in Cowie et al. (2004) and in the A370 field in I. Wold et al. (2012, in preparation). The remainder come from an ongoing campaign of follow-up spectroscopy in our fields using the DEep Imaging Multi-Object Spectrograph (DEIMOS) on the Keck telescope (L. Cowie 2011, private communication).

In Figure 1(a), we show H-band absolute magnitude versus redshift, where black points represent the spectroscopic sample and red points represent photometric redshifts (see Section 3). In Figure 1(b), we show the spectroscopic redshifts in our fields. The black histogram shows the total for all six fields, and the colored histograms show each field individually.

For our redshifts obtained with the Hydra instrument (1155 total), we assigned a simple confidence flag to the determined redshift to indicate whether it was a high-confidence redshift (1) or questionable (0). In reality there may be some ambiguity, in relatively low signal-to-noise spectra, as to when one can robustly determine a redshift versus when a redshift may be determined but could be questionable. To keep things simple in this case, we assign high confidence to redshifts where a minimum of two absorption or emission features could be clearly identified in different parts of the spectrum simultaneously. We assign questionable confidence when one or more features appear identifiable in a spectrum, such that a redshift could be defined, but that other possible fits to the spectrum cannot be completely ruled out. With this system we assign high confidence to ~92% of the redshifts in our Hydra sample.

3. SPECTRAL ENERGY DISTRIBUTION FITTING USING GAZELLE

We used the GAZELLE code (R. Kotulla et al. 2012, in preparation) to fit the SEDs of our target galaxies in order to obtain photometric redshifts for galaxies that lack spectroscopy. The GAZELLE code uses the GALaxy EEvolution (GALEV; Kotulla et al. 2009) stellar population synthesis models as the

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⁹ http://iraf.noao.edu/tutorials/dohydra/dohydra.html
basis for fitting SEDs. *GALEV* is an evolutionary synthesis code that allows the user to generate models to describe the evolution of stellar populations in general, whether they are resolved populations (as in the case of star clusters) or unresolved populations in galaxies.

Given a set of initial conditions, *GALEV* is able to track the integrated light properties of galaxies over cosmological timescales. Users are now able to generate their own models directly via the *GALEV* Web site (http://www.galev.org). To generate a model, the user first chooses a galaxy type (E, Sa, Sb, Sc, Sd) or specifies a particular star formation history (e.g., constant, exponentially declining, etc.), including an option to upload a user-defined star formation history.

*GALEV* is unique among evolutionary synthesis codes in that it allows the user to select a “chemically consistent” treatment by simultaneously tracking the spectral evolution of stellar populations and the chemical evolution (metallicity) of the gas component of galaxies. Alternatively, one can choose from five fixed metallicities in the range $-1.7 < \text{[Fe/H]} < +0.3$. The user may also vary the initial mass function (IMF), switch on or off the emission from gas, choose a Galactic extinction prescription, and vary parameters regarding the details of star formation efficiency and burst duration, age, $e$-folding time, etc., for starburst models. Lastly, the user chooses a cosmological parameter set, desired outputs of the model, and the photometric filter profiles to be applied to model SEDs.

In an effort to fit model SEDs to photometric data, a wide selection of models is required to cover a range of star formation histories, ages, metallicities, galaxy types, and so on. In this work, we chose 83 independent *GALEV* models to use in fitting our photometry. Twenty of these models are the types available through the *GALEV* Web site for five galaxy types (E, Sa, Sb, Sc, and Sd). Each galaxy type is modeled at three fixed metallicities ($\text{[Fe/H]} = -0.7, -0.3, 0$) and once in the “chemically consistent” evolving metallicity format. The other 63 models are starburst models that attempt to capture a wide range in post-burst age. The starburst models are not publicly available through the *GALEV* Web site. They are described in detail in the dissertation of Ralf Kotulla and were provided to us directly by him. Altogether, we use burst models covering 21 age steps (post-burst 0.002–9 Gyr) at three fixed metallicities ($\text{[Fe/H]} = -0.7, -0.3, 0$).

*GALEV* does not yet handle emission from dust, so that in low-redshift samples such as this work, the longer wavelength *Spitzer* bands contribute relatively little to the SED fits. This is because the *GAZELLE* code ignores photometry in bands where dust emission is expected to dominate the signal ($>3 \mu m$).

*GAZELLE* uses a $\chi^2$ algorithm to fit models to the observed data. The $\chi^2$ values for each model are then transformed into normalized probabilities. The model with the highest probability is the one chosen for computing redshift, mass, metallicity, and so on. The formal 1σ uncertainties in redshift, mass, metallicity, etc., are derived by finding the minimum and maximum values associated with the models in the top 68% of the normalized probability distribution.

*GAZELLE* includes an option to run with a user-defined redshift for galaxies. This mode allows the user to “calibrate” *GAZELLE* given the difference between observed photometry and the output model photometry from the best-fit SED. In this mode, we compared the output model magnitudes from *GAZELLE* with the input observed magnitudes and found very good agreement in the optical ($|m_{\text{observed}} - m_{\text{model}}| < 0.03$), but systematic offsets of $\sim 0.1$–0.2 in the NIR. We then included these offsets in the *GAZELLE* input parameter file to account for these systematics, such that, when we re-ran the code, the model output magnitudes agreed with the input magnitudes in all bands with systematics of $<0.03$ mag. These adjustments served to improve the spectroscopic versus photometric redshift relation.

At the relatively low redshifts of our sample, the error in photometric redshifts can be of the same order as the redshifts themselves. Despite these relatively large uncertainties, we find that the photometric redshifts derived for galaxies that lack spectroscopy fall within the range of expected values from the spectroscopic sample. We note that $>50\%$ of our targets have $|z_{\text{spec}} - z_{\text{phot}}|/(1 + z) < 0.05$ and $>80\%$ have $|z_{\text{spec}} - z_{\text{phot}}|/(1 + z) < 0.1$, which could be considered fairly typical for determining photometric redshifts.

4. THE NIR LUMINOSITY FUNCTION

The NIR LF of galaxies has been relatively well established at low redshifts of $(z) \sim 0.025$–0.06 (Cole et al. 2001; Kochanek et al. 2001; Jones et al. 2006). At slightly higher redshifts of $(z) \sim 0.06$–0.1, large surveys have also provided constraints on the LF and tend to arrive at a normalization that is a factor of $\sim 1.5$ times higher than lower redshift studies (Bell et al. 2003; Eke et al. 2005; Smith et al. 2009; Hill et al. 2010).

At the mean redshift of our sample $(z \sim 0.2)$ the LF is not particularly well constrained because, in this redshift range, depth and wide area are simultaneously required to sample the entire LF. Furthermore, high spectroscopic completeness is essential at these redshifts to overcome possible biases and to avoid the relative uncertainty in photometric redshifts.

![Image of H-band absolute magnitude vs. redshift for all galaxies in our sample.](image-url)

**Figure 1.** (a) $H$-band absolute magnitude vs. redshift for all galaxies in our sample. Black points represent the spectroscopic redshift sample and red points represent the photometric redshift sample. (b) All redshifts in our six fields. The total for all six fields is shown as a black histogram and each field is represented individually with colored histograms.

(A color version of this figure is available in the online journal.)
(σ_i/z ~ 1), which lead to large uncertainties in absolute luminosities.

Here we combine our fields to study the NIR LF normalization at 0.1 < z < 0.3 and to compare with lower redshift values. As noted above, our sample is selected in the H band, but we have photometry for the entire sample in the J and K bands as well (presented in Keenan et al. 2010b). Thus, we are able to derive LFs in J, H, and K to compare with a wide range of selections from the literature.

First, we derived LFs for the combination of all six of our fields in the H band using four different estimators for both the LF and its normalization. From these methods we devise a hybrid scheme of deriving the LF that combines two different LF estimators. We compute the J-, H-, and K-band LFs in this way to compare the overall shape and normalization with other studies from the literature. In the range 0.1 < z < 0.3, we have 812 galaxies. This subsample is 92% spectroscopically complete. The only other study to focus specifically on the NIR LF in this redshift range was performed by Feulner et al. (2003). Our sample represents a factor of four increase in the number of galaxies used in their work.

4.1. Methods for Calculating the Luminosity Function

Several methods exist for calculating the LF of galaxies. The most commonly assumed functional form of the LF is that of the Schechter (1976) function, which takes the following form:

\[ \Phi(L) dL = \phi^* \left( \frac{L}{L^*} \right)^\alpha \exp \left( -\frac{L}{L^*} \right) dL, \]  

which may be converted to be in terms of absolute magnitudes:

\[ \frac{L}{L^*} = 10^{-0.4(M-M^*)}, \]

such that

\[ \Phi(M) = 0.4 \ln(10) \phi^* \left( \frac{10^{0.4(M-M^*)}}{\Phi(M^*)^{\alpha+1}} \right) \exp \left( -\frac{10^{0.4(M-M^*)}}{\Phi(M^*)} \right). \]

The Schechter function parameter \( L^* \) (or \( M^* \)) represents the luminosity of galaxies at the knee of the LF, while \( \phi^* \) determines the number density of \( L^* \) galaxies, and \( \alpha \) is the faint-end slope. Methods for deriving the LF include parametric and non-parametric forms. In this work, we use a hybrid combination of parametric and non-parametric estimators to determine the Schechter function parameters, but first we compare four methods of LF estimation independently.

4.2. Parametric LF Estimation

The most commonly used parametric method is that of Sandage et al. (1979, STY). This method employs a maximum likelihood estimator (MLE) and the assumption that the LF takes the Schechter function form. An advantage of this method is that no binning is required. Instead, a probability density, \( p(M_i, z_i) \), is calculated for each galaxy with absolute magnitude \( M_i \) at redshift \( z_i \), where \( M_{\text{lim}}(z_i) \) is the faintest galaxy visible in an apparent magnitude-limited survey at redshift \( z_i \), such that

\[ p(M_i, z_i) = \frac{\Phi(M_i)}{\int_{M_{\text{lim}}(z)}^{M_i} \Phi(M') dM'}. \]

The likelihood function is then the product of the probability densities for all galaxies in the survey:

\[ \mathcal{L} = \prod_i p(M_i, z_i). \]

This product is maximized to obtain the best-fit Schechter function parameters. In this method, the density functions cancel in the calculation of the probability densities. Thus, this technique is insensitive to density inhomogeneities, and the normalization (\( \phi^* \)) must be determined via some other method.

4.3. Non-parametric LF Estimation

Non-parametric LF estimators include binned and non-binned methods, and no a priori assumption of the LF functional form is required. However, for purposes of comparison with other studies and other methods a Schechter function is usually fit to the resulting LF estimation.

The simplest non-parametric approach is the \( 1/V_{\text{max}} \) method of Schmidt (1968). This method assumes a homogeneous distribution of galaxies, such that each galaxy is assigned a weight \( 1/V_{\text{max}} \) based on the fraction \( V_{\text{max}} \) of the total survey volume in which that galaxy can be observed, given its absolute magnitude. The sum of the weights for galaxies in an absolute magnitude bin is then the number density, \( \Phi(M) \), for that bin. This method has the advantage that the normalization of the LF is determined directly, but it has been shown that this method may underestimate the number density of galaxies near the flux limit of a sample (Page & Carrera 2000).

Another non-parametric approach is the \( C^- \) method of Lynden-Bell (1971). The \( C^- \) method does not require binning, and it does not require the assumption of a homogeneous distribution of objects. Thus, as for STY, the normalization must be determined by other means. In the \( C^- \) method, the cumulative luminosity function is given by

\[ \phi(M_k) = \int_{-\infty}^{M} \Phi(M) dM = \psi_l \prod_i C_k (M_i) + 1. \]

In a sample with a redshift lower limit of \( z_{\text{min}} \), the value for the parameter \( C_k \) for each galaxy at \( (M_k, z_k) \) is the total number of galaxies that are both brighter than \( M_k \) in absolute magnitude and within the redshift range \( (z_{\text{min}} < z_k < z_{\text{lim}}) \), where \( z_{\text{lim}} \) is the maximum redshift that a galaxy with absolute magnitude \( M_k \) may be observed in the survey. In other words,

\[ C_k (M_k) = \sum_{i} W(M_k), \]

where the window function \( W(M_k) \) is defined as

\[ W(M_k) = \begin{cases} 1, & M < M_k \text{ and } z_{\text{min}} < z_k < z_{\text{lim}}; \\ 0, & \text{otherwise}. \end{cases} \]

The resulting cumulative luminosity function may then be binned and fit with a Schechter function for comparison with other studies.

Another popular non-parametric approach is the “Step-Wise Maximum Likelihood” estimator (SWML; Efstathiou et al. 1988). This method requires binning but no a priori assumption of homogeneity. In this case, the LF is parameterized into \( N_p \) steps of width \( \Delta M \) such that

\[ \Phi(M) = \Phi_k, \quad k = 1, \ldots, N_p. \]
The only method that establishes the normalization is the \(1/V_{\text{max}}\) method, so all four methods have been set to that normalization for comparison.

(A color version of this figure is available in the online journal.)

Two window functions, \(W(x)\) and \(H(x)\), are defined such that

\[
W(x) = \begin{cases} 
1, & -\Delta M/2 \leq x \leq \Delta M/2 \\
0, & \text{otherwise}
\end{cases} \quad (10)
\]

\[
H(x) = \begin{cases} 
1, & x > \Delta M/2 \\
(x/\Delta M + 1/2), & -\Delta M/2 \leq x < \Delta M/2 \\
0, & x < -\Delta M/2
\end{cases} \quad (11)
\]

Maximizing the likelihood function (please see Efstathiou et al. 1988 for details) then yields the following form of the differential LF:

\[
\Phi_k(M)\Delta M = \frac{\sum_i W(M_k - M_i)}{\sum_i (H_{\text{lim}}(M_k) - M_i)} \quad (12)
\]

This estimator is then applied iteratively, each time replacing the input values for \(\Phi_k\) with the output \(\Phi_k\) values from the previous iteration until sufficient convergence is achieved.

4.4. Comparison of Four LF Estimators

In Figures 2 and 3, we compare the LFs and Schechter function parameters \(M^*\) and \(\alpha\) determined from the four LF estimators described in Sections 4.2 and 4.3 (\(1/V_{\text{max}}\), STY, SWML, and \(C^-\)).

Figure 2 shows a comparison of the \(H\)-band LF derived for our sample using the four different methods. The \(1/V_{\text{max}}\) method is shown in black, the STY method in red, the SWML method in orange, and the \(C^-\) method in blue. The only method that establishes the normalization is the \(1/V_{\text{max}}\) method, so all four methods have been set to that normalization for comparison.

Figure 3 shows a comparison of the \(H\)-band LF parameters \(M^*\) and \(\alpha\) derived for our sample using the four different methods. The same color designations apply as for Figure 2.

We expect the \(\alpha\) parameter for our work to be close to the value of \(\alpha \approx -1\) found in large low-redshift studies, as evolution in the LF should be minimal since \(z \sim 0.2\). Given our comparison of different methods above, we decided to use the STY method to determine the \(\alpha\) parameter in the sections that follow. We determine the error in our calculation of \(\alpha\) by fitting a two-dimensional Gaussian to the distribution of values for the likelihood function in \(\alpha, M^*\) space. We find that a two-dimensional Gaussian is a good fit to the distribution. The respective 1\(\sigma\) error ellipse of the four methods of this Gaussian are shown in Figure 3.

In further exploration of fitting \(\alpha\) with STY, we found that the method is sensitive to the input apparent magnitude limit of the survey. Our sample is \(H\)-band selected, such that the magnitude limit is well known in the \(H\) band but less well defined in the \(J\) and \(K\) bands. Thus, we first determine \(\alpha\) in the \(H\) band \((\alpha = 0.91 \pm 0.11)\) and then hold that value fixed in our determination of \(M^*\) using STY for \(J\), \(H\), and \(K\).

In Section 5, we discuss a comparison with the COSMOS cone mock catalogs to study cosmic variance. We use the mock catalogs to test our method of determining \(\alpha\) and \(M^*\) with STY. To do this we combined all the mock catalogs to form a simulated survey 24 times the size of our survey. We applied the above methods to determine \(\alpha\) and \(M^*\). We then created mock surveys of six random sightlines the same size as our survey and performed the same process to test whether the values for \(\alpha\) and \(M^*\) recovered from the smaller survey were consistent with the global values. We found that the recovered values for \(\alpha\) and \(M^*\) for the smaller mock surveys were in 1\(\sigma\) agreement with the global values determined from combining all the mock catalogs.

4.5. Determining The LF Normalization

Of the four methods discussed above for determining the LF Schechter function parameters, the \(1/V_{\text{max}}\) method is the only one that gives the normalization directly. The other methods require that the normalization be determined by other means.

Several methods have been developed for determining the LF normalization, and these are studied in detail by Willmer (1997) via simulated data. Willmer (1997) found that the various density estimators yield roughly equivalent results and all tend to underestimate the true density of objects by some \(\sim 20\%\). The parameter \(\phi^*\) is related to the mean density \((\bar{\rho})\) of the sample...
through

\[ \phi^* = \frac{\pi}{\int_{M_{\text{min}}}^{M_{\text{max}}} \phi(M) dM}, \]

where \( M_{\text{bright}} \) and \( M_{\text{faint}} \) are the absolute magnitude limits of the survey.

One commonly used method for determining the mean density is the minimum variance estimator of Davis & Huchra (1982):

\[ n_{\text{minvar}} = \frac{\sum_{i=1}^{N} w(z_i)}{\int dV S(z) w(z)}, \]

where \( N_{\text{gal}} \) is the number of galaxies in the sample, \( S(z) \) is the selection function, and \( w(z) \) is a weighting function for the galaxy defined by the inverse of the second moment \( \langle J_3 \rangle \) of the two-point correlation function, \( \xi(r) \).

The selection function, \( S(z) \), is defined as

\[ S(z) = \frac{\int_{M_{\text{min}}}^{M(z)} \phi(M) dM}{\int_{M_{\text{min}}}^{M_{\text{max}}} \phi(M) dM}, \]

where \( M(z) \) is the faintest absolute magnitude detectable at redshift \( z \).

The weighting function is defined as

\[ w(z) = \frac{1}{1 + \pi J_3 S(z)}, \quad J_3 = \int_0^r r^2 \xi(r) dr. \]

In the case that all weights are set to a value of 1, the minimum variance estimator described above reduces to the so-called \( n_3 \) estimator proposed by Davis & Huchra (1982):

\[ n_3 = \frac{N_T}{\int_0^{z_{\text{max}}} S(z) dV}. \]

Another estimator proposed by Davis & Huchra (1982) is

\[ n_1 = \frac{\left[ \int_0^{z_{\text{max}}} N(z) dV \right]}{\left[ \int_0^{z_{\text{max}}} dV \right] z_{\text{max}}} \]

which in the case of 1 galaxy bin\(^{-1}\) reduces to the form used by Efstathiou et al. (1988):

\[ n_1 = \frac{1}{V} \sum_{i=1}^{N_{\text{gal}}} \frac{1}{S(z_i)}. \]

We show a comparison of the normalization derived using the aforementioned mean density estimators of Davis & Huchra (1982) alongside the result for the 1/\( V_{\text{max}} \) method in Table 2. In all cases, we have determined \( \alpha \) and \( M^* \) using the STY method. We find that all four estimates of the LF normalization agree to within 1\( \sigma \) statistical errors.

### 4.6. A Hybrid Method for Determining the NIR LF

All LFs for our observed data presented in the following sections are calculated using the method described in Section 4.4, where, using STY, we first determine \( \alpha \) from the \( H \)-band sample and then \( M^* \) for each bandpass. We then determine \( \phi^* \) by fitting a Schechter function to the 1/\( V_{\text{max}} \) results in each bandpass with \( \alpha \) and \( M^* \) fixed at the values determined with the STY method.

The 1/\( V_{\text{max}} \) method requires binning. Thus, we compared results from bin sizes ranging from 0.2–1 mag. We found the results to be consistent to within 1\( \sigma \) (statistical uncertainty in the resulting Schechter function fit). We settled on a bin size of 0.4 mag to provide the best counting statistics over a wide range in absolute magnitudes.

The STY method does not allow for any test of goodness of fit between data and model. We fit the Schechter function parameter \( \phi^* \) to the 1/\( V_{\text{max}} \) binned data, with \( \alpha \) and \( M^* \) fixed, using the \textit{mpfit.pro} least-squares fitting procedure of Markwardt (2009), which is based on the \textsc{MINPACK}\(^{10}\) of Jorge Moré. The resulting fits yield a \( \chi^2 \sim 15.5 \) for 10 degrees of freedom, suggesting that the Schechter function is a good fit to the data at the ~90\% confidence level. In Section 5, we discuss the systematic uncertainties in our determination of the LF normalization due to cosmic variance.

To calculate absolute magnitudes we modified the observed apparent magnitude by a distance modulus (DM), a \( K \)-correction \( K(z) \), and an evolution correction \( E(z) \), such that \( M = m - DM(z) - K(z) + E(z) \).

### 4.7. NIR \( K \)-corrections \( K(z) \)

At low redshifts, \( K \)-corrections are small and nearly independent of galaxy type in the NIR (Mannucci et al. 2001). Using SDSS and UKIDSS data, Chilingarian et al. (2010) showed that, at low redshifts \( z < 0.5 \), accurate \( K \)-corrections may be calculated using low-order polynomials and inputs of only redshift and one observed NIR color. They provide a \( K \)-correction calculator,\(^{11}\) which we used to compute \( K \)-corrections for galaxies in our sample given redshifts and NIR colors.

We find the calculator output values to be in agreement with the expected NIR \( K \)-corrections for galaxies at these redshifts derived by Mannucci et al. (2001). Given the analysis of Chilingarian et al. (2010) in comparing their calculator outputs with more rigorous \textsc{SFD} fitting methods for determining \( K \)-corrections, we expect that our magnitude errors associated with the \( K \)-corrections should be \( < \pm 0.1 \).

### 4.8. Evolution Corrections \( E(z) \)

Evolution in the rest-frame NIR for galaxies at relatively low redshifts is expected to be weak but still has a significant effect on the normalization of the LFs, particularly at \( z > 0.1 \). The simplest form of the evolution correction is \( E(z) = Qz \) (e.g., Smith et al. 2009), where \( Q \) is a positive constant. Blanton et al. (2003) showed that in the NIR, \( Q = 1 \) agrees well with

### Notes.

\(^{a}\) All \( \phi^* \) values are given in units of \( h^3 \) Mpc\(^{-3} \).

\(^{b}\) The four methods listed are 1/\( V_{\text{max}} \), plus three methods \( (n_{\text{minvar}}, n_1, n_3) \) used by Davis & Huchra (1982).

### Table 2

\( H \)-band NIR LF Normalization \( \phi^* \) Derived Using Four Different Methods\(^{b}\)

| Method          | \( \phi^* \times 10^3 \) |
|-----------------|--------------------------|
| 1/\( V_{\text{max}} \) | 15.3 ± 1.6               |
| \( n_{\text{minvar}} \) | 15.6 ± 1.4               |
| \( n_1 \)          | 14.9 ± 1.5               |
| \( n_3 \)          | 15.7 ± 1.3               |

\(^{10}\) http://www.netlib.org/minpack

\(^{11}\) http://kcor.sai.msu.ru/
stellar population synthesis models. Thus, for this work we adopt $Q_J = Q_H = Q_K = 1$, such that $E(z) = z$ in all bands.

4.9. The Correlation between Schechter Function Parameters

The Schechter function parameters $\phi^*$ and $M^*$ are correlated, as shown in Figure 4. Thus, rather than a direct comparison of $\phi^*$ values from various studies, we consider the product of the normalization and the characteristic luminosity ($\phi^* L^*$) in the following discussions of comparisons between our study and those from the literature.

The Schechter function parameter $\alpha$ is also correlated with $\phi^*$ and $M^*$ but uncorrelated with the product of the normalization and characteristic luminosity, as shown in Figure 5. Thus, our comparison of the product $\phi^* L^*$ between studies is unaffected by the variations in $\alpha$ from one study to another.

4.10. Comparing Studies with Different Photometric Methods

Here we briefly discuss the photometric methods employed in different studies that we compare with in this work. For all our photometry, we calibrate to 2MASS point sources and use the SExtractor (Bertin & Arnouts 1996) MAG_AUTO aperture, which fits a Kron-like (Kron 1980) ellipse to each galaxy. In Keenan et al. (2010b), we found that this aperture does an excellent job of retrieving the total magnitudes for galaxies at high signal to noise (galaxies in the current study are 4–5 mag above our detection limits of Keenan et al. 2010b).

In the case of Kochanek et al. (2001), Cole et al. (2001), Bell et al. (2003), Eke et al. (2005), and Jones et al. (2006), 2MASS Kron or similar apertures were used for photometry, and we expect this to be consistent with our work.

Hill et al. (2010) apply Kron aperture photometry to the UKIDSS Large Area Survey (LAS). Smith et al. (2009) also work with the UKIDSS LAS, but they use Petrosian magnitudes. They compare the difference between Petrosian and Kron magnitudes for ~7000 galaxies that also have photometry in 2MASS. They find that 2MASS Kron magnitudes are, in general, ~0.2 mag brighter than their UKIDSS Petrosian counterparts. We adjust the value for $M^*$ from Smith et al. (2009) to accommodate this difference.

Huang et al. (2003) use circular 8′′ apertures corrected to 20′′ apertures for galaxies at $K_{\text{Vega}} > 13$. While it is difficult to assess exactly how this method compares to our photometry, the errors on their measurement are large and so this does not affect our analysis. Similarly, the sample size of Feulner et al. (2003) is small enough that the associated uncertainties span essentially the entire range of measurements of $\phi^* L^*$ from the literature.

4.11. The Effects of Magnitude Errors on the LFs

The fundamental selection for this work comes from $H$-band photometry we obtained with the ULBCam (Hall et al. 2004) on the University of Hawaii 2.2 m telescope. Our final $H$-band mosaics are highly uniform and 4–5 mag deeper than the selection limit for this work ($H < 18$). We calibrated our photometry for all six fields using high signal-to-noise point sources in 2MASS and found no discernable systematics and a random magnitude error of $<0.05$. For the galaxies in this survey, which are extended and somewhat fainter than the calibration sources, our random magnitude error is $\sim 0.1$.

4.12. The Effects of Redshift Errors on the LFs

Our redshift sample consists of ~8% photometric redshifts and ~8% questionable spectroscopic redshifts. As demonstrated by comparison with the SDSS, the high-confidence spectroscopic sample could be considered accurate to within $\Delta z \sim 0.0005$. Thus, here we consider only the error associated with questionable and photometric redshifts.

If we assume, as an upper limit, that all questionable and photometric redshifts have an associated random error of $\Delta z/(1 + z) \sim 0.1$, then this would imply a random error in a calculated absolute magnitude of $\sim 1–1.5$. Although a large effect for any individual galaxy, the contribution of this effect to the mean magnitude error in any given magnitude bin would be
Figure 6. $J$-, $H$-, and $K$-band LFs of galaxies in our six fields combined for the redshift range $0.1 < z < 0.3$. We derived the parameters $M^*$ and $\alpha$ via the STY method and then applied the $1/V_{\text{max}}$ method and fit a Schechter function with $M^*$ and $\alpha$ fixed to derive the normalization $\phi^*$. In the left-hand panels (a, c, and e) we plot the entire LFs to show overall shape for comparison with lower redshift LFs from the literature. The colored lines show LFs from the studies denoted in the plots. In the right-hand panels, we zoom in on the normalization to highlight the differences between the normalization in this study and selections from the literature. The solid lines show the Schechter fits to the combined data for all six fields (five fields in the $K$-band where SSA17 lacks photometry). The error bars shown are the 1$\sigma$ Poisson errors taken from Gehrels (1986). The normalizations and $M^*$ values to the fitted Schechter functions for the combination of all six fields are given in Table 3.

(A color version of this figure is available in the online journal.)

4.13. The Effects of Evolution Corrections on the LFs

Cole et al. (2001) showed that for NIR LFs at $\langle z \rangle \sim 0.05$, the evolution correction has the effect of raising the normalization by $\sim 10\%$ and dimming $M^*$ by $\sim 0.1$ mag (though these changes were of the same order as their errors). Jones et al. (2006) did not apply an evolution correction for their sample at $\langle z \rangle \sim 0.05$, and they measure a significantly lower normalization and brighter $M^*$ than Cole et al. (2001). In general, however, applying an evolution correction does not significantly change the product of the normalization and characteristic luminosity ($\phi^* L^*$).

4.14. Effects of Magnitude Errors in General

The $E(z)$ and $K(z)$ errors, along with the aforementioned magnitude errors, amount to a total error in the calculated absolute magnitudes of $\sim 0.3$. If these errors are truly random, then the effect on the LFs will be to shift galaxies from one bin to another, but the randomness of the process should essentially cancel itself out.

4.15. The NIR Luminosity Function at $0.1 < z < 0.3$

In Figure 6, we show the $J$-, $H$-, and $K$-band LFs of galaxies in our six fields combined for the redshift range $0.1 < z < 0.3$. In the left-hand panels (a, c, and e), the entire LFs are shown to demonstrate the overall shape compared with lower redshift
Figure 7. Product of the Schechter function normalization and characteristic luminosity ($\phi^*L^*$) for NIR LFs in this study (filled circles) and selections from the literature. We have employed a color correction, such that all data from J, H, and K appear vertically on the same scale. We then normalized the $\phi^*L^*$ values to an error-weighted average of the large studies at $\langle z \rangle = 0.057$ of Cole et al. (2001) and Jones et al. (2006). All measurements from our study and from the literature for the J band are shown in blue, H band in green, and K band in red. In each case, $\phi^*L^*$ is plotted at the median redshift for galaxies in a given study. Where studies (including this one) have covered more than one bandpass, the J-band $\phi^*L^*$ is plotted at the median redshift of the study and H- and/or K-band values are shifted slightly along the abscissa for clarity. The error bars show the 1σ statistical errors in the product $\phi^*L^*$. The values for $\phi^*$ and $L^*(M^*)$ used to generate this figure are given in Table 3. The solid line shows the void radial density profile from Bolejko & Sussman (2011) that they claim could produce the apparent acceleration of the expansion of the universe observed via Type Ia supernovae. Bolejko & Sussman (2011) presented this void profile as a density contrast; $\langle \rho(r) \rangle / \rho_0$.

(A color version of this figure is available in the online journal.)

Selections from the literature. In the right-hand panels, we zoom in on the normalization ($M^* \sim -21.7$) to highlight the differences between this study and other studies from the literature. The solid lines show the Schechter fits to the combined data for all six fields (five fields in the K band where SSA17 lacks photometry).

Given the H-band value for $M^* \sim -21.7$, we can see from Figure 1 that we are sampling $M \sim M^*$ galaxies out to a redshift of $z \sim 0.3$. We also note from the distribution shown in Figure 1 that we do not have a significant number of $M \sim M^*$ galaxies below a redshift of $z \sim 0.1$, such that the normalization of the NIR LF is best sampled in this survey for $0.1 < z < 0.3$.

In Figure 7, we show the product of the LF normalization and characteristic luminosity ($\phi^*L^*$) as a function of redshift from this study (filled circles) and from some literature studies. All measurements in the J band are shown in blue, H band in green, and K band in red. We applied a color correction so that all three bandpasses would appear on the same scale vertically. We then normalized the $\phi^*L^*$ values to an error-weighted average of the large studies at $\langle z \rangle = 0.057$ of Cole et al. (2001) and Jones et al. (2006). In each case, $\phi^*L^*$ is plotted at the median redshift for galaxies in a given study. Where studies (including this one) have covered more than one bandpass, the J-band $\phi^*L^*$ is plotted at the median redshift of the study, and H- and/or K-band values are shifted slightly along the abscissa for clarity. The error bars show the 1σ statistical errors in $\phi^*$ for each study.

The solid black line in Figure 7 shows the void radial density profile from Bolejko & Sussman (2011), which they claim could produce the apparent acceleration of the expansion of the universe observed via Type Ia supernovae. Bolejko & Sussman (2011) present this void profile as a density contrast; $\langle \rho(r) \rangle / \rho_0$. We convert their density contrast profile to normalized $\phi^*L^*$ by normalizing to the average of the large low-redshift studies of Cole et al. (2001) and Jones et al. (2006). We note that such a radial density profile is not ruled out by current measurements of the NIR LF normalization.

We find that our measured value of the product $\phi^*L^*$ is $\sim 30\%$ higher than the mean value of studies at $\langle z \rangle \sim 0.05$. Our measurement could be considered a conservative underestimate of the true value of $\phi^*L^*$ for $0.1 < z < 0.3$ because our survey avoids known galaxy clusters in this redshift range.
5. COSMIC VARIANCE

The relative scatter in measurements of the NIR LF normalization over the past 10 years could be arising from a variety of sources, including differences in fitting or normalization methods, differences in $K(z)$ or $E(z)$ corrections, photometry errors or incomplete spectroscopy, and cosmic variance. Most likely, these differences arise from some combination of the aforementioned sources, but in the majority of modern surveys, cosmic variance accounts for a large fraction of the uncertainty budget. Thus, we wish to quantify and compare the effects of cosmic variance on the uncertainties in our measurements and those from the literature. First, we consider uncertainties due to cosmic variance in all recent measurements of the LF normalization in the literature.

5.1. Cosmic Variance in Recent Measurements of the NIR LF Normalization

Driver & Robotham (2010) have quantified cosmic variance for $M^*$ galaxies in the SDSS volume. They derive the following empirical formula to calculate the expected systematics due to cosmic variance in any low-redshift survey:

$$\text{Cosmic Variance} (\%) = \left[ 1.00 - 0.03 \sqrt{(A/B) - 1} \right] \times (219.7 - 52.4 \log_{10}(|AB \times 291.0|)) + 3.21(\log_{10}(AB \times 291.0))^2/\sqrt{NC/291.0}$$  \hspace{1cm} (20)

In the above formula, $A$ and $B$ are the transverse comoving lengths at the median redshift of the survey, and thus provide an aspect ratio $A/B$ for rectangular surveys ($A > B$). $C$ is the comoving length of the redshift interval surveyed, and $N$ is the number of independent sightlines composing the survey. Given this formula, it is clear that surveys with multiple sightlines suffer less from cosmic variance systematics (by a factor of $1/\sqrt{N}$) than single field surveys, and surveys with large aspect ratios are superior to those of square fields.

We calculated the expected systematics due to cosmic variance for each survey from the literature, given depth, area, aspect ratio, and number of fields as inputs to the empirical formula of Driver & Robotham (2010). We were not able to account for the fact that, in many cases, these surveys consisted of several sightlines, each having a different size and aspect ratio, so these estimates are not meant to be extremely rigorous, but rather to provide a means of comparing the relative effects of cosmic variance from one survey to the next. The results of this comparison are listed in Table 3. Below, we briefly discuss this estimate of cosmic variance in each survey from the literature.

The first efforts using large surveys to measure the local NIR LF normalization were Cole et al. (2001) and Kochanek et al. (2001). Both of these surveys used 2MASS for their NIR photometry, and Cole et al. (2001) used 2dFGRS spectroscopy for 5683 galaxies at a median redshift $z \sim 0.06$, while Kochanek et al. (2001) used the ZCAT data from the CfA2 redshift survey (Geller & Huchra 1989; Huchra et al. 1992) for 3878 galaxies at a median redshift $z \sim 0.023$. We find that both of these surveys should suffer from systematics due to cosmic variance at the $\sim 10\%$ level. Cole et al. (2001) estimate cosmic variance systematics at the $15\%$ level, using galaxy counts from 2MASS, and propagate this estimate through their error estimation.

Eke et al. (2005) provide an updated version of the study done by Cole et al. (2001) using 2MASS and the completed 2dFGRS to include 15,664 galaxies in the determination of the $K$-band LFs. Given the larger survey size, the estimated systematics due to cosmic variance in this sample are at the $\sim 6\%$ level.

The largest study to date of the local NIR LF was done by Jones et al. (2006). They combine 2MASS photometry with the 6-degree Field Galaxy Redshift Survey (6dFGS; Jones et al. 2004) to measure the $J$-, $H$-, and $K$-band LFs using $\sim 60,000$ galaxies at a median redshift $z \sim 0.054$. While this study includes more galaxies than previous works, the fact that it is relatively shallow implies that cosmic variance still persists at the $5\%$ level.

At median redshifts $z \sim 0.08$, Bell et al. (2003) and Hill et al. (2010) provide a measurement of the LF normalization. Bell et al. (2003) use a sample of 6282 galaxies selected from 2MASS.
with spectroscopy from the SDSS early data release. They find a normalization quite similar to that of Eke et al. (2005), though with larger error bars (cosmic variance at the $\sim 10\%$ level) due to the smaller sample size. Hill et al. (2010) combine the UKIDSS LAS, the SDSS, and the Millennium Galaxy Catalog (MGC; Liske et al. 2003) to form a highly uniform and 100% spectroscopically complete sample of $\sim 1800$ galaxies in the $J, H,$ and $K$ bands. Their LF normalization agrees well with that of Bell et al. (2003), though the relatively small volume of their sample implies possible systematics on the $\sim 30\%$ level due to cosmic variance.

Smith et al. (2009) use a sample of $\sim 40,000$ galaxies at a median redshift $z \sim 0.1$, drawn from the UKIDSS LAS with spectroscopy from the SDSS, to study the $K$-band LF. Their sample includes all UKIDSS LAS galaxies at $K_{\text{Vega}} < 16$ that have secure redshifts in the SDSS. While this is not a spectroscopically complete magnitude-limited sample, it is one of the largest samples used to study the $K$-band LF and samples a large volume. For this survey size, we estimate cosmic variance to be at the $2\%$. However, given the relative spectroscopic incompleteness, other biases may be a significant source of systematic uncertainties.

At median redshifts in the range $0.1 < z < 0.3$, very few studies of the NIR LF have been done. Furthermore, the relatively small sample sizes imply that measurements of the LF normalization over this range are subject to large systematic uncertainties due to cosmic variance. Huang et al. (2003) use a sample of 1056 galaxies to study the $K$-band LF at a median redshift of $z \sim 0.14$. Their measured normalization is essentially in agreement with all measurements at lower redshift, given their statistical errors plus cosmic variance at the $\sim 10\%$ level. Feulner et al. (2003) use a sample of 210 galaxies to study the $J$- and $K$-band LF at a median redshift of $z \sim 0.2$. The size of their survey implies uncertainties due to cosmic variance at the $\sim 30\%$ level, putting their measured normalization in agreement with all previous studies.

Our survey samples the same redshift range as Feulner et al. (2003), but our larger area and deeper completeness limits mean we have a factor of four more galaxies in our study, and the expected uncertainties due to cosmic variance have been reduced by a factor of two. As noted above, our measured normalization is in good agreement with studies at $z \sim 0.1$, but would appear to be in slight tension with studies at $z \sim 0.05$. In the following section, we explore the field-to-field variability in the LF normalization for our survey and compare with simulations using the COSMOS cone mock catalogs.

5.2. Cosmic Variance in Our Survey

We are measuring the normalization of the NIR LF over the redshift range $0.1 < z < 0.3$, or comoving distances of $\sim 300–850\, h^{-1}$ Mpc. Thus, with a total of $2\, \text{deg}^2$ on the sky we are sampling the normalization over a volume of $\sim 10^3\, h^{-3}$ Mpc$^3$. With typical large-scale structures existing on at least $\sim 100\, h^{-1}$ Mpc scales, we expect (and indeed find) significant field-to-field variation in the measured normalization.

In Figure 8, we show the $J$-, $H$-, and $K$-band LFs for $0.1 < z < 0.3$ on a field-to-field basis. In all cases the A370 field shows a much higher normalization than the other five fields, even though the A370 cluster itself, at redshift $z = 0.37$, is not included in these LFs. The solid black line shows Schechter fits to the combination of all six fields. The colored lines show Schechter fits for each of the six fields individually.

In Table 4, we give the normalizations for each field and the combination of fields in the range $0.1 < z < 0.3$. These values were calculated using the $1/V_{\text{max}}$ method and fitting a Schechter function with fixed $\alpha = 0.91$ from applying STY in the $H$ band and fixed $M^*$ values (given in Table 3 derived in each bandpass using STY with a fixed $\alpha = 0.91$).
We find agreement between the normalizations in all fields except the A370 field, where the normalization is a factor of ~2 higher. Upon investigation of this apparent excess, we find that two sheet-like overdensities exist in the A370 field at redshifts of $z \sim 0.18$ and $z \sim 0.25$ (both clearly visible in Figure 1). These overdensities are very narrow in redshift space, spanning the redshift ranges $0.17 < z < 0.19$ and $0.245 < z < 0.255$, respectively. To determine whether our survey appears to be consistent with cosmological simulations, and to further explore the expected systematics due to cosmic variance in this study, we use the COSMOS cone mock catalogs.

5.3. Comparison with The COSMOS Cones

The COSMOS cones are composed of 24 pencil beam mock catalogs created by Manfred Kitzbichler (Kitzbichler & White 2007) for the Cosmic Evolution Survey collaboration (COSMOS; Scoville et al. 2007b) and made public in the Millennium Database online. These catalogs were created from the Millennium Simulation (Springel et al. 2005) using the galaxy formation algorithm of De Lucia et al. (2006) and the merger tree prescriptions of De Lucia & Blaizot (2007). The COSMOS cone catalogs have been used primarily to study galaxy formation and evolution, as well as large-scale structure, at relatively high redshifts (Scoville et al. 2007a; McCracken et al. 2007; Knobel et al. 2009; Kovač et al. 2010). We use the catalogs here to compare with our observations of the NIR LFs at $0.1 < z < 0.3$.

The COSMOS cone mock catalogs represent eight sightlines from each of three different origins within the Millennium Simulation. Each of the COSMOS cone pencil beams covers an area of $1.4 \times 1.4$ deg, or ~2 deg$^2$. Thus, each mock catalog is roughly the equivalent area of our entire survey, and so we divide each mock catalog into six separate sightlines. This gives us a total of 144 mock sightlines to compare with our observations. K-band apparent magnitudes are provided in the mock catalogs (though not J or H band), so we take a magnitude-limited sample from the mocks of $K < 18$ to compare with our data.

From the 144 sightlines, we first select six at random. We show an example of the distribution in absolute $K$-band magnitude and redshift for six random sightlines selected from the COSMOS cones in Figure 9. This apparent magnitude selection of $K < 18$ typically generated a catalog of ~1500 objects in the combination of six sightlines. We note the similarity in the distribution of redshift and absolute magnitude in comparison to our observed data for $H < 18$ shown in Figure 1.

Next, we construct LFs to study the variability in the normalization from field to field. Rather than using the absolute magnitudes provided in the catalogs, we attempted to mimic our methodology applied to the observed data by using the apparent $K$-band magnitudes from the mock catalogs, and converting to absolute magnitude via a distance modulus, a $K$-correction from Mannucci et al. (2001), and an $E(z) = z$ correction. We then compared the normalization of the LFs in six randomly selected mock catalogs in the same manner as with the observational data, where we estimated $\alpha$ and $M^*$ with the STY method and then found the normalization fitting a Schechter function to the $1/V_{\text{max}}$ results with a fixed $\alpha$ and $M^*$.

We completed 1000 realizations of the process of selecting six sightlines at random and evaluating their LFs. We found that we have a ~25% chance of drawing a survey like ours, with one overdense sightline, from the mock catalogs. Thus, while the appearance of overdensities like those in the A370 field might not be characteristic of sightlines chosen at random from simulations, they are not strongly atypical. However, we note that in both observations and simulations, massive galaxy clusters tend to lie at the confluence of large filamentary structures, such that choosing to observe in the direction of a

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|}
\hline
Field & $\phi^* \times 10^3$ & $\phi_{H}^* \times 10^3$ & $\phi_{K}^* \times 10^3$ \\
\hline
All Fields & $15.9 \pm 1.7$ & $15.3 \pm 1.6$ & $14.6 \pm 1.7$ \\
A370 & $24.4 \pm 4.9$ & $23.1 \pm 4.7$ & $23.0 \pm 4.5$ \\
CLANS & $14.4 \pm 3.5$ & $13.9 \pm 3.4$ & $12.7 \pm 3.1$ \\
CLASXS & $12.0 \pm 3.3$ & $11.5 \pm 3.2$ & $10.3 \pm 2.8$ \\
CDF & $10.9 \pm 6.4$ & $12.5 \pm 7.4$ & $10.4 \pm 6.3$ \\
SSA13 & $17.3 \pm 7.7$ & $15.5 \pm 7.7$ & $15.3 \pm 7.6$ \\
SSA17 & $13.3 \pm 5.6$ & $15.0 \pm 6.2$ & N/A \\
\hline
\end{tabular}
\caption{NIR Luminosity Function Normalizations$^a$ in Each of Six$^b$ Fields for the Redshift Range $0.1 < z < 0.3$}
\end{table}

Notes.
$^a$ All $\phi^*$ values are given in units of $h^3$ Mpc$^{-3}$. These values were calculated using the $1/V_{\text{max}}$ method and fitting a Schechter function with fixed $\alpha = 0.91$ from applying STY in the $H$ band, and fixed $M^*$ values given in Table 3 derived in each bandpass using STY with a fixed $\alpha = 0.91$. This method is described in Section 4.4.
$^b$ Only five fields in the case of the K band where the SSA17 field lacks photometry.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure9.png}
\caption{(a) Redshift vs. $K$-band absolute magnitude in an example selection of galaxies ($K < 18$) for the combination of six sightlines of 1/3 deg$^2$ each taken at random from the COSMOS cone mock catalogs. (b) A histogram of all redshifts in the six mock catalogs. The solid black line shows the total over six fields and the colored lines represent the six fields individually. We note the similarity in the distribution of redshift and absolute magnitudes in these example mock catalogs in comparison to our observations shown in Figure 1. (A color version of this figure is available in the online journal.)}
\end{figure}

\footnote{http://gavo.mpa-garching.mpg.de/MyMillennium3/Help?page=databases/mpamocks/cosmos2006}
galaxy cluster may increase the chances of finding overdensities along the line of sight.

Next, we measured the expected systematic uncertainty due to cosmic variance by looking at the distribution of measured normalizations for our 1000 mock surveys of six sightlines. We find that the distribution is well fit by a Gaussian (see Figure 10) with a 1σ variability of ∼13% in the measured normalization over the 1000 combinations of six random sightlines.

We repeated the process of 1000 realizations of simulated surveys with the number of sightlines (1/3 deg² each) ranging from 1–30. Also shown in Figure 10 is the distribution in measured normalization for surveys of 12 and 24 sightlines for comparison.

In Figure 11, we show the 1σ systematic uncertainty (in percent) due to cosmic variance as a function of the number of sightlines for each mock survey drawn from the COSMOS cones. The expected systematics given by the empirical formula of Driver & Robotham (2010) are shown as a solid line. We find that the two estimates agree rather well, and hence we confirm their results derived from observed data with our analysis of the COSMOS cones. Given these results, we find that doubling the number of sightlines in our survey should reduce the effects of cosmic variance to the ∼10% level, while quadrupling the survey should reduce these systematics to the ∼5% level.

6. SUMMARY

An accurate measurement of the average space density of galaxies just beyond the local universe (z > 0.1) is of interest, in particular, because recent cosmological modeling efforts have shown that if the matter density at z < 0.1 is low by roughly 50%, then the apparent acceleration of the expansion of the universe observed in Type Ia supernovae could simply be a product of our location with respect to local structure (Alexander et al. 2009; Bolejko & Sussman 2011).

We have presented a study of the NIR LF normalization at redshifts of 0.1 < z < 0.3. This study is based on a highly complete (>90%) spectroscopic sample of 812 galaxies, selected to be brighter than 18th magnitude in the H band, over six widely separated fields at high Galactic latitudes. While consisting of a relatively small sample of galaxies, our survey represents a factor of four increase in the number of galaxies in previous studies of the NIR LF in this redshift range, which implies a factor of two decrease in the systematic uncertainties due to cosmic variance.

We construct the NIR LFs for each field individually and for the combination of all six fields. We compare the product of the normalization and characteristic luminosity (Φ∗ L∗) in the combination of our six fields with lower redshift measurements to test for a higher luminosity density at z > 0.1. We find our measurement of Φ∗ L∗ to be in agreement with other studies at median redshifts near z ∼ 0.1, but roughly 30% higher than the error-weighted mean at ⟨z⟩ ∼ 0.05. Our measurement of Φ∗ L∗ for 0.1 < z < 0.3 could be considered a conservative underestimate of the true value of Φ∗ L∗ because we avoid known galaxy clusters in this redshift range.

We use the COSMOS cone mock catalogs and the empirical formula of Driver & Robotham (2010) to investigate the effects of cosmic variance on our measurement of the NIR LF normalization and on those from the literature. Despite the uncertainties due to cosmic variance, it would appear that data from the literature are beginning to suggest a rising luminosity density from z = 0.05 to z = 0.1. While this conclusion is tentative at best, it would not be terribly surprising, as a rising LF normalization over this redshift range would be predicted given the results of several NIR galaxy count surveys over the past 10–20 years.
More importantly, however, we require knowledge of the luminosity density at \( z > 0.1 \) to understand whether or not the local universe is underdense. We find that measurements of the NIR LF at \( z > 0.1 \), including our own, are still too uncertain to provide a robust comparison with lower redshift measurements. While inconclusive, this result is noteworthy given the possible implications for locally measured cosmological observables.

Surveys that are currently underway, including our own campaign of spectroscopic follow-up on fields that have existing NIR photometry, will soon provide a more robust answer to the question of whether or not we reside in a large local underdensity.

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