Simulation Research of Potential Contrast Agents for X-Ray Fluorescence CT with Photon Counting Detectors

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XFCT is a novel method for the early cancer detection. Increasing concentration of contrast agents and incident X-rays' energy were used to improve detecting accuracy, which greatly increased the prevalence of contrast-induced nephropathy. Therefore, this research explores the adaptive contrast agents and uses Geant4 to simulate the imaging conditions of Pt, Bi, Gd, Ru, and Au for searching the lowest detectable concentration based on the fast multi-pinhole collimated XFCT (fmpc-XFCT) imaging system and low incident energy. Several imaging parameters including pinhole radius (0.7, 0.8, and 1 mm) were adjusted, and the optimized EM-TV algorithm was used to reconstruct XFCT images. It is found that Bi element is superior to other metal elements in terms of the contrast-to-noise ratio (CNR) and fluorescence efficiency, and the lowest concentration that can be detected is 0.12% with optimal parameters.

Keywords: fmpc-XFCT system, contrast agents, CNR, fluorescence efficiency, lowest concentration

INTRODUCTION

X-ray fluorescence computed tomography (XFCT) is a novel method to detect early-stage cancer, combining X-ray computed tomography (X-CT) with X-ray fluorescence technology (XRF) [1–3]. For conventional X-CT imaging, the reconstructed image is the absorption coefficient of incident X-ray, which is difficult to distinguish the diseased and normal tissue for the slight difference of absorption. XFCT can be seen as a stimulated emission tomography, which can determine the spatial distribution of the contrast agents [4].

However, the development of XFCT is mainly limited by the high radiation dose and low detection sensitivity when used for an in vivo image. Increasing the concentration of contrast agent and incident X-rays' energy was to solve this problem, which greatly increased the prevalence of contrast-induced nephropathy (CIN). CIN has become the third cause of iatrogenic kidney injury, which not only prolongs hospitalization and medical expenses but also increases the risk of death, especially for the venerable and diabetics. The preventive measures for CIN include hydration therapy, selecting hypotonic or isotonic contrast agents, reducing the dose of contrast agents, and supplying speed [5]. Therefore, the essential measure is to reduce the concentration of the contrast agents.

However, there is no specific contrast agent for XFCT, which mainly used the X-CT contrast agent like gold nanoparticles (GNPs). Liu et al., used Pt as the XFCT contrast agent and verified its
feasibility by the Monte Carlo simulation [6]; Gd was commonly used as the X-CT and MRI contrast agent, and Zhang et al. used it for XFCT and figured out that the number of fluorescence photons of Gd is two times more than that of Au and imaged it at a sub-mg/mL level [7]; Li et al. proposed Ru nanoparticles as the contrast agent of XFCT, and the lowest detectable concentration is 0.2 mg/ml [8]. At the same time, they also proposed other potential fluorescent materials such as Y, Zr, Nb, Rh, and Bi [9]. The systems mentioned above are traditional scanning and rotating systems with long scanning time and high radiation dose. This manuscript explores the minimum dosage of scanning and rotating systems with long scanning time and high radiation dose. Then the flux rate, $I_t$, detected by the detector is obtained by the following equation:

$$I_t = \int_{-\infty}^{\infty} f(a, s, t) g(a, s, t) dt,$$  \hspace{1cm} (2)

where the $f(a, s, t)$ and $g(a, s, t)$ are shown as follows:

$$f(a, s, t) = I_0 \exp \left[-\int_{-\infty}^{\infty} \mu^t(s, t') dt' \right],$$  \hspace{1cm} (3)

$$g(a, s, t) = \mu \phi \omega \int_{ym}^{ym} \exp \left[-\int_{-\infty}^{\infty} \mu^s(s-b \sin \gamma, s+b \cos \gamma) db \right] d\gamma,$$  \hspace{1cm} (4)

$f(a, s, t)$ represents the process of incident X-ray reaching the point Q and $g(a, s, t)$ represents the process of fluorescent X-ray radiated from the point Q reaching the detector. $a$ and $s$ denote the angle and the translation offset of the incident X-ray, respectively. $\mu$ is the photoelectric linear attenuation coefficient of contrast agents. $\omega$ is the angle at the point Q viewed by the detector.

In the research, we ignore the constant term and discretize the phantom into $M \times N$ pixels. Consequently, Eq. 2 can be simplified as follows:

$$I = Hd,$$  \hspace{1cm} (5)

$$H = f g L \quad (1 \leq i \leq M, 1 \leq j \leq N),$$  \hspace{1cm} (6)

where $f_{ij}$ means the attenuation of the $ith$ incident X-ray passing through the $jth$ pixel; $g_{ij}$ means the attenuation of the fluorescent X-ray; $L_{ij}$ is the intersection length of the $ith$ X-ray and the $jth$ pixel.

During the reconstruction process, $I$ and $H$ are known, and $d$ in the equation is to be solved.

**Reconstruction Algorithm**

Maximum likelihood-expectation maximization (ML-EM) is an estimation method for solving unknown parameters in the likelihood function based on the maximum likelihood criterion. The maximum likelihood criterion requires, under certain test conditions, the optimal estimation value of the unknown parameter to be the sampling result reaching the maximum probability. Accordingly, the optimal estimation value could provide the likelihood function the maximum value. The iterative formula in reconstruction is as follows:

$$d_{i+1} = d_i + \sum_{j} h_{ij} \sum_{k} h_{ik} d_k,$$  \hspace{1cm} (7)

where $d_i$ means the estimated value of $d$ pixel after the $kth$ iteration and $h_{ij}$ is the projection matrix, which means the weight of the $ith$ detector from the $jth$ pixel.

In order to further improve the quality of the reconstructed images, we adopt the optimized ML-EM algorithm proposed by
Zhang et al. [13] and add the total variation term (TV) as a penalty function [14] to reduce the background noise. The optimized EM-TV algorithm is expressed as follows:

\[
\begin{align*}
I_{SCA} &= \int_D f_{\text{co}} \exp \left(-\int_{Q}^{R} \mu^{c}(s, t) \, ds \right) d(s, t) \mu_{co} \\
& \times f_{\text{KN}}(E, \theta_{\text{SCA}}) \int_{Y} \exp \left(\int_{Q}^{R} \mu^{s}(s, t) \, ds \right) \, dy \, dt,
\end{align*}
\]

where \(\theta_{\text{SCA}}\) is the scattering angle, \(\mu_{\text{CO}}\) is the Compton scattering cross-section, and \(f_{\text{KN}}\) is the Klein–Nishina formula, which can be obtained as follows:

\[
f_{\text{KN}}(E, \theta) = \frac{\pi r^{2} \sin \theta \left(1 + \cos^{2} \theta \right)}{\left[1 + \alpha (1 - \cos \theta)\right]^{2}} \times \left(1 + \frac{\alpha (1 - \cos \theta)^{2}}{\left(1 + \cos^{2} \theta \right) \left[1 + \alpha (1 - \cos \theta)\right]}\right)
\]

The iterative formula in reconstruction is as follows:

\[
d^{k+1}_{ij} = \frac{d^{k}_{ij}}{\sum_{i=1}^{m} h^{(XRF)}_{ij}} \sum_{i=1}^{m} h^{(XRF)}_{ij} \frac{I^{(ALL)}_{ij}}{\sum_{i=1}^{m} (h^{(XRF)}_{ij}d^{k}_{ij} + h^{(SCA)}_{ij}S^{k}_{ij})},
\]

where

\[
I^{(ALL)}_{ij} = I^{(XRF)}_{ij} + I^{(SCA)}_{ij},
\]

\[
S^{k+1}_{ij} = \frac{S^{k}_{ij}}{\sum_{i=1}^{m} (h^{(SCA)}_{ij}d^{k}_{ij} + h^{(SCA)}_{ij}S^{k}_{ij})}
\]

Note that \(I^{(XRF)}\) and \(I^{(SCA)}\) are the fluorescent projection and scattering noise projection, respectively; \(d^{k}_{ij}\) and \(S^{k}_{ij}\) are the mean estimated values of concentration and noise of the \(j\)th pixel after the \(k\)th iteration; \(h^{(XRF)}_{ij}\) and \(h^{(SCA)}_{ij}\) are the mean fluorescent projection matrix and the scattering projection matrix, respectively.

In reality, the stability and robustness of the algorithm will decrease due to a large number of iterations. Hence, the acceleration factor is introduced to improve the convergence of the algorithm.

\[
d^{k+1}_{ij} = d^{k}_{ij} - \alpha \omega v,
\]

where \(\alpha\) is the gradient descent relaxation factor, and \(\omega\) is the gradient descent scale parameter, whose value belongs to \([0, 1]\). The large value of \(\omega\) will cause the image to be too smooth, but the over smaller value will reduce the calculation speed [15]. In this study, we set \(\omega\) equal to 0.2. \(v\) as the gradient descent direction, which is approximately the partial derivative of total variation of the image:

\[
\frac{\partial \|d\|_{TV}}{\partial d_{ij}} = \frac{(d_{ij} - d_{i,j+1}) + (d_{ij} - d_{i,j-1})}{\sqrt{\varepsilon + (d_{ij} - d_{i,j+1})^2 + (d_{ij} - d_{i,j-1})^2}} - \frac{d_{i,j+1} - d_{ij}}{\sqrt{\varepsilon + (d_{i,j+1} - d_{ij})^2}}
\]

where \(\varepsilon\) is a positive number for fidelity and preventing the denominator from being 0. Normally, \(\varepsilon\) is an empirical parameter, which is set to a very small number. Here, we set \(\varepsilon = 10^{-8}\).

**Image Quality Evaluation**

Here, we use the contrast-to-noise ratio (CNR) [16] as an objective criterion to evaluate reconstructed images, which is defined as follows:

\[
\text{CNR} = \frac{|\Psi_{A} - \Psi_{B}|}{\sigma_{bk}}
\]

where \(\Psi_{A}\) is the average value of pixels in ROIs, \(\Psi_{B}\) is the average value of background pixels, and \(\sigma_{bk}\) is the standard deviation of the pixel values of the background area.

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**FIGURE 2** Fast multi-pinhole collimated XFCT system.
EXPERIMENT

The experimental system is the fmpe-XFCT imaging system proposed by the authors, which is not needed to be translated and rotated, and imaged by fan beam scanning once [10]. The system settings are shown in Figure 2.

The imaging system includes an X-ray source, a phantom, two sets of multi-pinhole collimators, and two sets of detectors. Two sets of photon counting detectors are to obtain projections under double incident photons, thereby reducing the radiation dose. The distance between the X-ray source and the center of the sample is 15 cm (AO), the distance between the collimator and the sample is 5 cm (B1O and B2O), and the distance between the detector and the collimator is also 5 cm (B1C1 and B2C2). The detector consists of $55 \times 185$ detector crystals made of CdTe, the energy resolution is 0.5 keV, the crystal size is $0.3 \text{ mm} \times 0.3 \text{ mm}$, and the center distance of the detection crystal is 0.5 mm. The multi-pinhole collimator is made of Pb with a thickness of 5 mm. There are three pinholes with a radius of 1 mm for a set of multi-pinhole collimator. The pinhole is formed by superimposing two cones with a bottom angle of 55°. To avoid overlapping projections on the detectors, the vertical distance between the holes is 1.5 cm. The system is placed in the air.
Simulation Settings

In this study, a phantom with a radius of 2.5 cm was proposed: a small cylinder was filled with contrast agents (Pt, Bi, Gd, Ru, and Au), with a radius of 1.5 mm, a height of 5 cm, and concentrations of 0.2, 0.4, 0.6, 0.8, 1.0, and 1.2%, as shown in Figure 3. It was called high-concentration phantom, abbreviated as HCP. It was used to explore the lowest concentration of the contrast agents.

This experiment is based on the Rose criterion, that is, ROI can be detected when $\text{CNR} \geq 4$ [17].

In this experiment, we simulated the energy distribution of X-ray tube source in SpekCalc [18], using low-energy incident X-rays to excite the sample to reduce the radiation dose and Compton scattering (tube voltage = 62 keV).
RESULTS AND DISCUSSION

Results
In this experiment, the fluorescent materials were set as Pt, Bi, Gd, Ru, and Au. The projection data were obtained by Geant4 simulation, and the ML-EM algorithm was used for reconstruction. The reconstructed images are shown in Figure 4: for picture (A), the ROI brightness is poor and indicates concentration differences badly; for (B)–(D) all perform well, concentration differences are better, the ROI boundary is clear, the internal uniformity is excellent, and the distinction between each ROI is clear; and for (E), the inside of the ROI has poor uniformity and boundary clarification. For low-concentration ROI, neither can be distinguished well.

Therefore, we changed ML-EM to the optimized EM-TV algorithm. The reconstructed images are shown in Figure 5. The ROIs in (A)–(E) are well dispersed, the boundaries of each ROI are clear, and the interior is uniform, and the shape is closer to phantom, which means the higher reconstructed capability. For (B) and (D), each of ROI is circular, and its reconstructed shape achieves the best. For (E), there is adhesion between the ROIs and blurred edges. From the subjective evaluation, the image quality of Bi and Ru has better performance, and the image quality of Au is the worst. CNR is used to evaluate image quality objectively,
and it shows that the CNR value increases with the increase of concentration, as shown in Figure 6. For lower concentrations, Ru and Bi have a greater advantage (0.2–0.6%). Gd has a better performance for high concentrations. For each of the concentration, the CNR value of Au is the smallest, and its performance is the worst.

For different fluorescent materials, the fluorescence efficiency is an important factor. The average value of each ROI is to be represented by its fluorescence photons, exploring the fluorescence efficiency. We fit the variation of the ROI average value with concentration and use its slope to characterize its fluorescence efficiency. Figures 7–11 shows the fitted curves of different contrast agents. Gd has the highest fluorescence efficiency, followed by Bi, and Ru has the lowest fluorescence efficiency. Considering CNR and fluorescence efficiency, Bi as the contrast agent is optimal.

**Discussion**

The above experiments show that Bi has a good performance. In order to further explore its imaging potential, we change the concentration as shown in Figure 12 (low-concentration phantom, LCP) and adjust the collimated hole radius to 0.8 and 0.7 mm (originally 1 mm). The reconstructed images of optimized EM-TV are shown in Figures 13A–C.
For the image with a small hole radius of 1 mm, the ROI is the brightest, which is the best image among the three apertures. It can also be concluded that the aperture with 1 mm size can get the best result in terms of CNR for detecting low concentrations, and the minimum detection limit is 0.12%; for 0.14, 0.16, and 0.2%, the aperture 0.07 mm performs best; at 0.18%, the aperture 0.08 mm performs best.

The shortcoming of this experiment is that we do not take the self-absorption effect into consideration that makes the reconstructed image distorted slightly. And for the fmpc-XFCT system, it may get the worst performance when the concentration of contrast agent reaches a relatively low level, that is, <0.1%.

CONCLUSION

We simulated Pt, Bi, Gd, Ru, and Au as the fluorescent materials of the fast XFCT imaging system. Gd has the highest fluorescence efficiency, and the quality of the reconstructed images is the best for high concentration, and the performance is poor for low concentration, so it can be used to detect the tumor shape when the concentration is high to determine the treatment plan; Pt and Ru perform well in concentration resolution, but their low fluorescence efficiency limits their detection effect; for Au as an contrast agent, its reconstructed images' quality limits the application; and Bi performs well in image quality and fluorescence efficiency. Therefore, Bi is a highly potential fluorescent material. In addition, the solubility of the Bi mixture is small in most solvents. Therefore, after entering the human body as a drug, it is not easy to penetrate into the human tissue and most can be metabolized easily, making it suitable for in vivo imaging.

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DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/Supplementary Material; further inquiries can be directed to the corresponding authors.

AUTHOR CONTRIBUTIONS

The research was designed by LY, FP, and ZY, and the research funds were provided by FP, AK, ZY, and HP. The experiments were made by LY and ZR. The manuscript was written by LY and revised by FP, YS, and ZX.

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**Conflict of Interest:** The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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