Infrared spectroscopy of the $\nu_2$ band of the water monomer and small water clusters (H$_2$O)$_n$=2,3,4 in helium droplets

Raffael Schwan, Matin Kaufmann, Daniel Leicht, Gerhard Schwaab and Martina Havenith*

We have recorded infrared spectra in the frequency range of the $\nu_2$ band of water monomer and water clusters in superfluid helium droplets. In order to be able to map the chemically important fingerprint range, we have used an IR quantum cascade laser as a radiation source. We were able to observe three ro-vibrational transitions of the water monomer between 1590 and 1670 cm$^{-1}$. The lines were assigned to the $1_{00} \rightarrow 1_{01}, 1_{15} \rightarrow 0_{00}$ and $2_{12} \rightarrow 1_{01}$ transitions of the $\nu_2$ vibration of H$_2$O. Based upon the linewidths, we could deduce relaxation times of 1.9 to 4.2 ps for the monomer. Additional absorption bands could be assigned to $\nu_2$ vibrational bands of water clusters (H$_2$O)$_n$ with $n$ = 2, 3, 4. These experimental results are compared to theoretical calculations by Wang and Bowman which are reported in an accompanying paper [ref. 1, Y. Wang and J. M. Bowman, Phys. Chem. Chem. Phys., 2016, DOI: 10.1039/C6CP04329A]. We find a very good agreement of our results with both calculations and with previous results from gas phase cavity ringdown experiments.

Introduction

A molecular understanding of water–water interactions is a crucial endeavor for the advancement of modern science and has, therefore, been subject of numerous experimental and theoretical studies. For the water monomer, gas phase reference data of the H$_2$O$_{16}$ isotopomer cover a total of more than 12 000 ro-vibrational states$^5$ and more than 25 000 ro-vibrational transitions have been assigned.$^5$ To describe the water–water interactions quantitatively, many detailed studies of small water clusters [(H$_2$O)$_n$ with $n$ = 2–10] have been published in recent articles and reviews.$^5$ Of particular relevance to the present study are the measurements including IR spectroscopic studies in helium nanodroplets$^8$–$^{12}$ and gas phase cavity ringdown experiments in supersonic beams.$^{13}$–$^{17}$ In addition, numerous spectroscopic studies of isolated water clusters in noble gas matrices$^{18}$–$^{24}$ as well as many theoretical studies$^{25}$–$^{30}$ have been carried out in the past few decades. The most recent investigations on the structure of water clusters (H$_2$O)$_n$ with $n$ = 6–10 were performed using broadband rotational spectroscopy$^6$ and terahertz VRT spectroscopy.$^7$

Helium droplets provide a unique soft matrix for spectroscopic measurements.$^{31}$–$^{33}$ They offer the possibility to study single molecules or clusters under ultracold, well-defined conditions. The temperature of helium droplets has been found to be 0.37 K.$^{34}$ At this temperature only a small number of rotational states in the vibrational ground state of the embedded species are populated. It has been found that molecules can rotate freely in helium droplets.$^{31}$–$^{33}$ For light molecules (e.g. water monomer) with rotational constants $B_{\text{gas}} > 1$ cm$^{-1}$, only weak coupling with the helium is expected while for heavy rotors with $B_{\text{gas}} < 0.5$ cm$^{-1}$ (e.g. SF$_6$)$^{35}$ rotational constants are typically reduced by a factor of three compared to the gas phase.$^{32}$–$^{33}$

Previously, the IR spectra of water in helium droplets have been reported for the $\nu_1$ and $\nu_3$ stretch vibrations.$^{10}$–$^{12}$ Here, we report IR spectra of water clusters embedded in helium nanodroplets showing the $\nu_2$ bending vibration. We have expanded the frequency range by integrating quantum cascade lasers (QCL) into our setup. IR OPO systems are restricted to frequencies above 2500 cm$^{-1}$, which excludes the chemically important fingerprint region. Nowadays, narrow band tunable quantum cascade lasers allow probing of the frequency range between 600 cm$^{-1}$ and 2500 cm$^{-1}$. The principle of quantum cascade lasers has first been described by Faist $et$ $al.$ in 1994.$^{36}$ The main advantage of quantum cascade lasers is that the wavelength can be tuned within the same semiconductor material over a wide spectral range. Using different semiconductor materials, a large part of the mid-infrared region$^{16}$–$^{40}$ as well as parts of the THz region$^{41}$ can be covered. Continuous wave (CW) operation of a QCL at room-temperature has been first described by Beck$^{42}$ in 2002. Nowadays, widely tunable QCL systems are commercially available using an external cavity configuration.$^{13}$ First measurements employing a quantum cascade laser as a radiation source...
for spectroscopy in helium nanodroplets have been reported by the groups of Douberly and Momose at around the same time in 2011. In this work, we report spectroscopic measurements with a tunable external cavity quantum cascade laser (EC-QCL) on our helium nanodroplet spectrometer in Bochum. The experimental results are compared to theoretical predictions by Bowman and co-workers in an accompanying paper.1

Experimental

The experimental setup of the helium nanodroplet beam apparatus used in this study is explained in detail elsewhere. Briefly, helium droplets are formed by the expansion of ultra-pure $^4$He 5.0 through a pre-cooled nozzle with a diameter of 5 μm to vacuum. Here, we used a stagnation pressure of 60 bar and a nozzle temperature of 16 K. A 0.5 mm skimmer collimates the evolving helium droplet beam. The helium droplets are doped with water molecules in a differentially pumped pickup chamber connected to the expansion chamber. Small amounts of water are added to the chamber via a dosing valve.

For the measurements in this work, a tunable EC-QCL (Daylight Solutions) was used which emits light between 1570 and 1720 cm$^{-1}$ with an output power of 50–230 mW. The laser beam is superposed with the molecular helium nanodroplet beam in an antiparallel configuration. The infrared radiation excites ro-vibrational transitions of the dopants inside the helium droplets. The ro-vibrationally excited molecules relax into the ground state by releasing energy to the helium droplets resulting in evaporation of helium atoms (about 5 cm$^{-1}$ per atom). The depleted helium droplets are ionized and detected by a mass spectrometer (Pfeiffer QMG 422). The mass spectrum shows characteristic fragment signals for the doped species and its aggregates.

By observing the ion current of one of these fragments separately, mass-selective absorption spectra can be recorded. However, different aggregates can decompose into fragments with equal mass-to-charge ratios. In these cases, the recorded absorption spectrum is a superposition of the absorption spectra of the individual aggregates. A lock-in amplifier allows phase-sensitive detection at the frequency of the amplitude modulated laser beam.

Results

Observation of the $\nu_2$ band of H$_2$O monomer

Fig. 1 shows the depletion spectra for ionic fragments observed in the mass spectrum at $m/z = 18$, 19 and 37. The ion current at $m/z = 18$ corresponds to the ionic fragment (H$_2$O)$^+$, $m/z = 19$ to [H(H$_2$O)]$^+$ and $m/z = 37$ to [H(H$_2$O)$_2$]$^+$. The IR depletion spectrum detected at $m/z = 18$ shows a total of five peaks (Fig. 1a). By comparison with gas phase data, three lines are assigned to ro-vibrational transitions of the water monomer.

For light rotors all rotational constants are well above the temperature of the helium droplets, thus, only the lowest ro-vibrational state will be populated at 0.37 K. However, due to slow spin conversion in helium droplets, spin statistical weights are conserved during the internal cooling of the molecules embedded in helium nanodroplets. For the water monomer, there are two different nuclear spin species, para and ortho, for which the spin statistical weights are 1:3, respectively. The water monomer is an asymmetric rotor with ground-state rotational constants of $C_0 = 9.2877 \pm 0.0021$ cm$^{-1}$, $B_0 = 14.5074 \pm 0.0090$ cm$^{-1}$ and $A_0 = 27.8761 \pm 0.0034$ cm$^{-1}$ in the gas phase. The Boltzmann distribution at 0.37 K allows only the energetically lowest ro-vibrational states of each
nuclear spin species to be populated, namely 000 and 101. Therefore, the number of transitions that can be observed is restricted to transitions from these two populated levels. All allowed ro-vibrational transitions from these two states are shown in Fig. 2 (solid lines).

In previous publications, the symmetric and asymmetric stretch vibrations \( \nu_1 \) and \( \nu_3 \) of the water monomer in helium droplets have been observed.\(^{10,11}\) Here, we focus on the \( \nu_2 \) bending vibration. We report the observation of three ro-vibrational transitions at 1616.1, 1634.9 and 1654.4 cm\(^{-1}\), which are assigned to the b-type 101 \( \leftrightarrow \) 000, 111 \( \leftrightarrow \) 000 and 122 \( \leftrightarrow \) 010 transitions of the \( \nu_2 \) band, respectively. The line positions, the linewidths and the deduced lifetimes as determined by the fit to a Lorentzian line shape are shown in Table 1. The b-type ro-vibrational lines are separated by \( \approx 2C_0 \) each, yielding an estimate for the rotational constant. We obtain a rotational constant \( C_{\text{He}} = 9.56 \pm 0.23 \text{ cm}^{-1} \) which is slightly higher than the experimentally observed gas phase rotational constant \( C_0 = 9.2877 \pm 0.0021 \text{ cm}^{-1}.\(^{51}\) A similar observation was made by the Vilesov group who have reported a rotational constant \( C_{\text{He}} = 9.5 \text{ cm}^{-1} \) for the \( \nu_3 \) band of water.\(^{11}\) Since the effect of the superfluid helium environment on the rotational constant \( C \) is very small, we assume the same for the rotational constants \( A \) and \( B \) along the \( \nu_2 \) band.

(caption: Fig. 2. Energy level diagram for the water monomer. The labels of the rotational states are following the nomenclature for asymmetric rotors \( J_{\text{alc}} \) with their association to ortho and para spin states. In superfluid helium nanodroplets only the lowest lying rotational state for each spin state, i.e. 101 (ortho) and 000 (para), is populated. IR active b-type (left) and a-type (right) transitions from the lowest populated states are displayed as solid lines. Dashed arrows indicate possible pathways for rotational relaxation. Relaxation processes are restricted to relaxations within the same spin state. Adapted from ref. 11.)

| Line       | Gas phase \( \text{cm}^{-1} \) | He \( \text{cm}^{-1} \) | \( \delta \nu \) | \( \tau \) [ps] |
|------------|---------------------------------|--------------------------|---------------|--------------|
| \( \nu_3 \) |                                 |                          |               |              |
| 101 \( \leftrightarrow \) 000 | 1616.7 | 1616.1 | 1.3 | 4.2 |
| 111 \( \leftrightarrow \) 000 | 1635.0 | 1634.9 | 1.7 | 3.2 |
| 122 \( \leftrightarrow \) 010 | 1653.3 | 1654.4 | 2.8 | 1.9 |
| \( \nu_4 \) |                                 |                          |               |              |
| 101 \( \leftrightarrow \) 010 | 3674.7 | 3674.3\(^{b} \) | 2.4\(^{b} \) | 2.2 |
| 111 \( \leftrightarrow \) 000 | 3693.3 | 3693.1\(^{b} \) | 3.0\(^{b} \) | 1.8 |
| 122 \( \leftrightarrow \) 010 | 3711.4 | 3711.4 | —     | —           |
| \( \nu_5 \) |                                 |                          |               |              |
| 000 \( \leftrightarrow \) 101 | 3732.1 | 3732.0\(^{b} \) | 0.34\(^{b} \) | 15.6 | 17.7 |
| 010 \( \leftrightarrow \) 000 | 3779.5 | 3778.2\(^{b} \) | 0.34\(^{b} \) | 0.26 | 15.6 | 20.6 |
| 020 \( \leftrightarrow \) 010 | 3801.4 | 3809.9\(^{b} \) | 2.3\(^{b} \) | 1.9 | 2.3 | 2.8 |

\(^{a}\) From ref. 3. \(^{b}\) From ref. 11. \(^{c}\) From ref. 10.

Table 2. Rotational relaxation channels in the \( \nu_2 \) excited vibrational level of the water monomer and their associated energy gaps \( \Delta \nu \). The energy gaps have been calculated from the gas phase rotational constants

| Initial \( J_{\text{KaKc}} \) | Final \( J_{\text{KaKc}} \) | \( \Delta \nu \) [cm\(^{-1}\)] |
|-----------------------------|-----------------------------|-----------------------------|
| 101                         | 110                         | 18.6                       |
| 111                         | 000                         | 37.2                       |
| 122                         | 110                         | 37.2                       |
| 212                         | 101                         | 55.8                       |

The deduced lifetimes of the excited ro-vibrational states are in the range between 1.9 to 4.2 ps as summarized in Table 1. These values can be compared to previous observations for the \( \nu_1 \) and \( \nu_3 \) stretch bands.\(^{10,11}\) While for the \( 2_{02} \) \( \leftrightarrow \) 101 a-type transition a lifetime of 2.8 ps has been deduced, the 101 \( \leftrightarrow \) 000 and 000 \( \leftrightarrow \) 101 a-type transitions of the \( \nu_3 \) band have lifetimes which exceed this value by one order of magnitude (see Table 1). This observation is explained by a lack of lower rotational states with the same symmetry in the excited vibrational state, thus, excluding population relaxation of the excited states 101 and 000.\(^{10,11}\) All excited ro-vibrational states of the b-type transitions observed in this work as well as the excited state 202 of the a-type transition of the \( \nu_3 \) band can relax rotationally to lower lying states (see Fig. 2, dashed lines). The energy gaps between the distinct rotational states are in the range \( \approx 18-56 \text{ cm}^{-1} \) (see Table 2). We want to point out that the line position of the 111 \( \leftrightarrow \) 000 transition shows virtually no shift compared to the gas phase (1634.9 \text{ cm}^{-1} \text{ versus} 1635.0 \text{ cm}^{-1}). The small increase of \( C \) is considered to be an artifact due to the restricted number of rotational lines.

We want to point out that the line position of the 111 \( \leftrightarrow \) 000 transition shows virtually no shift compared to the gas phase (1634.9 cm\(^{-1}\) versus 1635.0 cm\(^{-1}\)). The small increase of \( C \) is considered to be an artifact due to the restricted number of rotational lines.

Observation of the \( \nu_2 \) band of water clusters (H\(_2\)O\(_n\), \( n = 2, 3, 4 \))

The depletion spectrum recorded at \( m/\Delta z = 19 \), which corresponds to the ion fragment ([H\(_2\)O\(_n\)]\(^+\)), shows four peaks at 1600.5, 1608.5, 1614.8 and 1629.1 cm\(^{-1}\) (Fig. 1b). The peaks at 1600.5 and 1614.8 cm\(^{-1}\) are also observed in the depletion spectrum recorded at \( m/\Delta z = 18 \) (Fig. 1a). In order to unambiguously assign these peaks to a specific cluster size we have recorded the pressure dependence.
The pickup probability of molecules by helium droplets can be described by a Poisson distribution.\(^{31,32,55}\) The probability \(P_n\) to embed \(n\) molecules into a helium droplet with the capturing cross section \(\sigma_{\text{cap}}\) in a pickup-chamber of length \(L\) is described as:

\[
P_n = A \left( \frac{(p - p_0)}{k_B T} \sigma_{\text{cap}} L \right)^n \exp \left( - \frac{(p - p_0)}{k_B T} \sigma_{\text{cap}} L \right)
\]

with an amplitude \(A\) and a pressure offset \(p_0\) that takes into account the residual water in the chamber. The pressure offset \(p_0\) and the product of the capturing cross section \(\sigma_{\text{cap}}\) and the length \(L\) are adjusted to describe the pressure dependence of the dimer bands at 1600.5 and 1614.8 cm\(^{-1}\) and kept constant for the fits of the other bands.

The pressure dependence of the signals of the two spectral features at 1600.5 and 1614.8 cm\(^{-1}\) could be reproduced well by a Poisson distribution with \(n = 2\) (see Fig. 3). The assignment to \((\text{H}_2\text{O})_2\) is confirmed by the fact that these bands are observed at \(m/z = 18\) and \(m/z = 19\). The two bands at 1600.5 and 1614.8 cm\(^{-1}\) are assigned to the water bending mode of the proton acceptor and the proton donor of the water dimer, respectively. In Table 3 we summarize the center frequencies obtained for the gas phase and in helium nanodroplets and compare these to the theoretical predictions. Compared to the gas phase, we observe a red-shift (\(\approx 5.2\) cm\(^{-1}\)) of the bending mode for the proton donor, while virtually no shift for the proton acceptor is observed (\(\approx 0.1\) cm\(^{-1}\)). The band contour can be attributed to an underlying rotational fine structure of the bands (see Fig. 4). The rotational constants of the water dimer were determined as 7.02, 0.22 and 0.22 cm\(^{-1}\) by theoretical calculations on the B3LYP/cc-pVTZ level of theory. To simulate the experimental band contours, the rotational constants of 0.22 cm\(^{-1}\) were reduced by a factor of three to account for the effect of the surrounding helium, whereas the rotational constant of 7.02 cm\(^{-1}\) was assumed to be unaffected.

Based upon the pickup curves, the bands at 1608.5 and 1629.1 cm\(^{-1}\) are assigned to the water trimer (Fig. 3). For the water trimer, the global minimum structure, labeled 3(a) (see Fig. 5),
is cyclic. Each water molecule serves as a proton donor as well as a proton acceptor. Two of three free OH moieties are oriented up while the third is oriented down with respect to the ring. In Table 3 we compare the experimental and the predicted frequencies for the water trimer. The rotational constants of the water trimer were predicted to be 0.23, 0.23, 0.12 cm$^{-1}$ at the B3LYP/cc-pVTZ level of theory. For the predictions of the line contours, we assume a reduction of the rotational constants by a factor of three to account for the effect of the surrounding helium. The experimentally observed line broadening of the band at 1629.1 cm$^{-1}$ clearly exceeds the predicted rotational broadening. The experimentally observed line shape can be reproduced assuming two close-lying absorption bands separated by 1 cm$^{-1}$. The experimental result is in good agreement with the predictions of Wang and Bowman$^1$ who predict bands at 1617, 1619 and 1634 cm$^{-1}$ for the water trimer.

In order to search for absorption bands of larger clusters, we recorded an additional depletion spectrum at a higher pressure on mass $m/z = 37$, which corresponds to the ionic fragment $[\text{H(H}_2\text{O)}_n]^+$. Here, we expected to observe only water clusters $(\text{H}_2\text{O})_n$ with $n \geq 3$. Surprisingly, we also observed bands attributed to the water dimer in this spectrum, however, with decreased intensity. Based upon mass spectrometric observations, we propose that these are due to fragments of clusters of helium with $\text{H}_2\text{O}$ with the general formula $[\text{H(He)}_n]^+$.

The dimer bands at 1600.5 and 1614.8 cm$^{-1}$ are detected at $m/z = 37$ which corresponds to the ionic fragment $[\text{H(He)}_3]^+$. However, the intensity is considerably reduced compared to the intensity at $m/z = 37$, which corresponds to the ionic fragment $[\text{H(He)}_4]^+$.

![Fig. 4](image-url)  
Fig. 4 Experimentally observed bands of the water dimer $(\text{H}_2\text{O})_2$ and water trimer $(\text{H}_2\text{O})_3$ at $m/z = 19$. The observed bands are compared with the predictions assuming a Boltzmann distribution at 0.37 K. For the simulations of the water dimer $(\text{H}_2\text{O})_2$ and water trimer $(\text{H}_2\text{O})_3$ transitions, rotational constants of $A = 7.02$ cm$^{-1}$, $B = C = 0.07$ cm$^{-1}$ and $A = B = 0.08$ cm$^{-1}$, $C = 0.04$ cm$^{-1}$ were used, respectively. Lines were broadened assuming a Lorentzian line shape. The broad feature at about 1608.5 cm$^{-1}$ is explained by two overlapping bands in agreement with theoretical predictions.$^1$

The ro-vibrational fine structure was plotted using PGOPHER.$^{57}$

### Table 3

| $n$ | Experiment | Theory |
|-----|-------------|---------|
|     | He | Gas phase | Bowman |
| 1   | 1597.5 | 1594.7$^a$ |         |
| 2   | 1600.5 | 1600.6$^b$ | 1584$^c$ |
|     | 1614.8 | 1620$^b$ | 1607$^c$ |
| 3   | 1608.0 | 1609$^b$ | 1617 (0.12)$^d$ |
|     | 1609.0 | 1619 (0.09)$^d$ |         |
|     | 1629.1 | 1638$^b$ | 1634 (0.03)$^d$ |
| 4   | 1629.0 | 1629$^b$ | 1629 (0.09)$^d$ |
|     | 1641.2 | 1634 (0.06)$^d$ |         |
|     |       | 1634 (0.06)$^d$ |         |
|     |       | 1654 (0.0)$^e$ |         |

$^a$ From ref. 2. $^b$ From ref. 14. $^c$ From ref. 26. $^d$ From ref. 1.
curve recorded at 1629.1 cm\(^{-1}\) shows, for higher pressures, a clear deviation from the Poisson distribution for \(n = 3\) and resembles more a pressure dependence that would be expected for \(n = 4\). In addition, the contour of the band at 1629.1 cm\(^{-1}\) differs depending on whether we record the IR spectrum at \(m/z = 37\) or \(m/z = 19\). This supports the assignment of the broad feature to two overlapping bands.

Experimentally, the two water tetramer bands are found to be separated by about 12 cm\(^{-1}\). This value can be compared to calculations in the accompanying paper of Wang and Bowman\(^1\) who predicted a splitting of 5 cm\(^{-1}\). However, in their paper they argue that this value might be an underestimation since high-level direct \(ab\ initio\) calculations show a splitting of 12 cm\(^{-1}\) (compare to ref. 5c and 6 in Wang and Bowman\(^1\)), which is in good agreement with experiment.

The formation of the higher energy isomer, labeled 4(b) (see Fig. 5), can be excluded since the theoretical calculations for this isomer predict a band highly blue-shifted compared to the bands found experimentally. At higher pressures, the pickup curve at 1641.2 cm\(^{-1}\) deviates from the \(n = 4\) Poisson distribution and resembles more a distribution for \(n = 5\). Therefore, we propose a spectral overlap of the bands of the water tetramer with the bands of the water pentamer.

Two bands at 1600.5 and 1614.8 cm\(^{-1}\) were assigned to the water dimer (H\(_2\)O)_2 in good agreement with the bands at 1606.6 and 1620 cm\(^{-1}\) observed in the gas phase.\(^{14}\) The broadening of the lines can be explained by the underlying ro-vibrational fine structure. Furthermore, we have assigned three bands at 1608.0, 1609.0 and 1629.1 cm\(^{-1}\) to the water trimer (H\(_2\)O)_3. For higher water pressures, a broad absorption feature between 1620 and 1650 cm\(^{-1}\) arises. Within this absorption, two broad bands centered at 1629.9 and 1641.2 cm\(^{-1}\) could be assigned to the water tetramer (H\(_2\)O)_4. The experimental data are in good agreement with the theoretical predictions in the accompanying paper of Wang and Bowman.\(^1\)

Acknowledgements

We thank Y. Wang and J. Bowman for helpful discussions. We acknowledge financial support from the Cluster of Excellence RESOLV (EXC 1069) funded by the Deutsche Forschungsgemeinschaft.

References

1. Y. Wang and J. M. Bowman, \(Phys. Chem. Chem. Phys.\), 2016, DOI: 10.1039/C6CP04329A.
2. J. Tennyson, N. F. Zobov, R. Williamson, O. L. Polyansky and P. F. Bernath, \(J. Phys. Chem. Ref. Data\), 2001, 30, 735–831.
3. L. S. Rothman, R. R. Gamache, A. Goldman, L. R. Brown, R. A. Toth, H. M. Pickett, R. L. Poynter, J.-M. Flaud, C. Camy-Peyret, A. Barbe, N. Husson, C. P. Rinsland and M. A. H. Smith, \(Appl. Opt.\), 1987, 26, 4058.
4. F. N. Keutsch and R. J. Saykally, \(Proc. Natl. Acad. Sci. U. S. A.\), 2001, 98, 10533–10540.
5. A. Mukhopadhyay, W. T. S. Cole and R. J. Saykally, \(Chem. Phys. Lett.\), 2015, 633, 13–26.
6. J. O. Richardson, C. Pérez, S. Lobsiger, A. A. Reid, B. Temelso, G. C. Shields, Z. Kisiel, D. J. Wales, B. H. Pate and S. C. Althorpe, \(Science\), 2016, 351, 1310–1313.
