Magnetic entropy table-like shape and enhancement of refrigerant capacity in La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$–La$_{1.3}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$ composite

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In this work, we have investigated the structural, magnetic and magnetocaloric properties of La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ (A) and La$_{1.3}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$ (B) oxides. These compounds are synthesized by a solid-state reaction route and indexed with respect to Sr$_2$Ti$_2$O$_7$-type perovskite with the $I4/mmm$ space group. The substitution of La by 10% Eu enhances the value of magnetization and reduces the Curie temperature ($T_C$). It is also shown that these compounds undergo a first-order ferromagnetic–paramagnetic phase transition around their respective $T_C$. The investigated samples show large magnetic entropy change ($\Delta S_M$) produced by the sharp change of magnetization at their Curie temperatures. An asymmetric broadening of the maximum of $\Delta S_M$ with increasing field is observed in both samples. This behaviour is due to the presence of metamagnetic transition. The $\Delta S_M(T)$ is calculated for $A_x/B_{1-x}$ composites with $0 \leq x \leq 1$. The optimum $\Delta S_M(T)$ of the composite with $x = 0.48$ approaches a nearly constant value showing a table-like behaviour under 5 T. To test these calculations experimentally, the composite with nominal composition $A_{0.48}/B_{0.52}$ is prepared by mixing both individual samples A and B. Magnetic measurements show that the composite exhibits two successive magnetic transitions and possesses a large MCE characterized by two $\Delta S_M(T)$ peaks. A table-like magnetocaloric effect is observed and the result is found to be in good agreement with the calculations. The obtained $\Delta S_M(T)$ is $\approx 4.07 \, \text{J kg}^{-1} \, \text{K}^{-1}$ in a field change of 0 – 5 T in a wide temperature span over $\Delta T_{FWHM} \approx 68.17 \, \text{K}$, resulting in a large refrigerant capacity value of $\approx 232.85 \, \text{J kg}^{-1}$. The MCE in the $A_{0.48}/B_{0.52}$ has demonstrated that the use of composite increases the efficiency of magnetic cooling with $\mu_0H = 5 \, \text{T}$ by 23.16%. The large $\Delta T_{FWHM}$ and RC values together with the table-like ($-\Delta S_M)^{\text{max}}$ feature suggest that the $A_{0.48}/B_{0.52}$ composite can meet the requirements of several magnetic cooling composites based on the Ericsson-cycle. In addition, we show that the magnetic field dependence of MCE enables a clear analysis of the order of phase transition. The exponent $N$ presents a maximum of $N > 2$ for A, B and $A_{0.48}/B_{0.52}$ samples confirming a first-order paramagnetic–ferromagnetic transition according to the quantitative criterion. The negative slope observed in the Arrott plots of the three compounds corroborates this criterion.

1. Introduction

Manganese oxides exhibiting colossal magnetoresistance (CMR) and large magnetocaloric effect (MCE) are a very hot topic in materials science, not only because of the interest they have generated in basic research but also for their potential technological applications in spintronics and magnetic refrigeration (MR). In addition, their adjustable phase transition temperatures, low-price and wear and corrosion resistance provide an additional advantage for the choice of manganese oxides as magnetic refrigerant materials for designing a “green” cooling refrigerator. Magnetic refrigerators are considered an ecologically friendly technology because of several advantages they have compared to traditional refrigerators. High efficiency, small volume, and being free of harmful gas leakage are among these advantages. The latter machines work on the principle of the MCE, which describes the adiabatic temperature change of magnetic substance produced by the magnetic entropy change ($\Delta S_M$) upon magnetization and demagnetization. When magnetics stimulus in an adiabatic process is applied, the entropy of the spin subsystem is diminished and the transfer of energy to the lattice produces heating of the magnetic substance. Conversely, removing magnetics stimulus of the substance causes it to cool down. The exploration of new refrigerant materials with large MCE at both ambient and
cryogenic temperatures is strongly desired and is vital in accelerating the progress of magnetic cooling technology. Nevertheless, large MCE and negligible thermal and magnetic-field hysteresis losses are required for MR. Considering the various requirements for applying magnetic cooling, La$_{2-x}$Ca$_{x}$Mn$_2$O$_7$ Ruddlesden–Popper phases ($n=2$) possess high magnetic moments and have a giant magnetocaloric effect. A giant peak value of $\Delta S_M$ (16.8 J kg$^{-1}$ K$^{-1}$) originating from the abrupt change of magnetization observed at 5 T in La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ system. This value is mostly close to that of systems undergoing a first order magnetic phase transition (FOMT) such as Gd$_3$GeSi$_2$ (18.5 J kg$^{-1}$ K$^{-1}$) and MnFeP$_2$As$_2$ (18 J kg$^{-1}$ K$^{-1}$) alloys under the same field change. Generally, the $\Delta S_M$ is adopted as an important index to demonstrate the refrigerant ability. Moreover, for a sample exhibiting FOMT, the value of $\Delta S_M$ is highest near the magnetic transition temperature and falls rapidly with temperature, making its usage limited over a narrow temperature range. Even though the change in magnetic entropy is large in such type of materials, they exhibit large thermal and field hysteresis on variation of magnetization with temperature and magnetic field, respectively. However, a considerable refrigerant capacity (RC), besides a giant peak entropy change, is also essential to obtain an excellent refrigeration efficiency. In this context, FOMT compounds do not seem to be the best choices, as their large hysteresis losses and limited temperature spans lead to significant decreases in refrigerant capacities. From the practical application point of view, materials with a large MCE over a broad temperature range are desired. However, it is therefore interesting to search for new FOMT materials with low-level hysteresis, high performance and excellent functional stability. Among the presently known MCE materials with a first-order magnetic transition (FOMT) the La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ compounds fulfill most of the requirements for practical applications of magnetic refrigeration. First, it has a limited thermal hysteresis at the FOMT. Second, it is easy to tune the operating temperature by varying the La/Ca ratio or by substituting the Mn ion by various transition metal. Furthermore, the composition of this compound is low priced, have good chemical stability, easy to prepare, and does not contain any toxic or expensive elements such as arsenic and germanium, respectively.

It is well known that the structure of La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ is constructed from ferromagnetic metal bilayer slices of MnO$_2$ sheets taken from the cubic perovskite, each slice being separated by a nonmagnetic insulating spacer layer which serves to isolate the bilayers (La, Ca)$_2$O$_3$ stacked along the c-axis. The anisotropy and the reduced dimensionality of these compounds play a crucial role in their special properties different from those shown by the cubic perovskites. Basically, the simultaneous ferromagnetic and metallic states observed in the Mn-based perovskite are explained using the double exchange mechanism (DE) caused by charge disproportionation. The DE interaction in the Mn–O–Mn network in the case of bilayer manganite is expected to be much weaker along the stacking c-axis direction because of the intervening rock salt layer that disrupts the interaction between the [MnO$_2$] layers. Members of this perovskite family are very responsive to small changes in composition and structure because of their layered structure. An inherent anisotropy modifies the thermomagnetic properties of the layered materials.

In the context of magnetic cooling, the La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ compound shows an abrupt change in the magnetization ($\partial M/\partial T$) and illustrates his magnetic entropy ($\Delta S_M(T)$) with particularly peak at Curie temperature. However, in regenerative Ericsson cycle, the entropy change of the refrigerant $\Delta S_M(T)$ should be constant (table-like MCE) over the operating temperature range of about 30 K. For this, there are number of publications in which the authors have proposed different solutions to improve the cooling capacity at larger spans. Therefore, a solution is to work with a multiphase or sandwich materials. These materials extend the temperature range in which the magnetic entropy changes significantly increase the possibility of improving performance through layering. Another simple way that increases the efficiency of magnetic cooling of bilayer manganites is the creation of the composite by a succession of magnetocaloric refrigerant samples with similar values of $\Delta S_M$ and refrigerant capacity (RC). In this work, an optimum molar fraction of La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ (A) and La$_{1.3}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$ (B) is determined for the assembling of a composite to be used as refrigerant material in solid-state magnetic cooling. A physical mixture of La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ and La$_{1.3}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$ is introduced to extend the operating temperature window because $T_c$ of La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ can be modified by small addition of Eu in La site. In addition, to extend the range of refrigeration, a composite magnetic refrigerant can be also used to increase or to optimize the refrigeration capacity (RC). This represents approximately the total thermal energy transferred from the hot to cold reservoirs over the active temperature range. Therefore, it was demonstrated that mixing of La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ (A) and La$_{1.3}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$ (B) provides an extra material design tool such that the optimal magnetic refrigerant material can be developed for a specific temperature range. The experimental results agree well with those calculated and discussed in the framework of an optimum regeneration Ericsson cycle. The MCE and RC of a prepared composite have been compared with those of individual bilayer manganites.

2. Experimental details

In this work, standard ceramic process is used to prepare two samples: La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ (sample A) and La$_{1.3}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$ (sample B). Well-grounded stoichiometric mixture of La$_{2}$O$_3$, MnO$_2$, CaCO$_3$ and Eu$_2$O$_3$ with a purity of (99.9%) is prepared. These contents are mixed and grounded, then sintered for 12 h at 1200 °C. Subsequently pressed into pellets, which and sintered again for 12 h at 1200 °C. After grinding, the annealed powders are then pressed into disks and sintered at 1400 °C for 12 h with intermittent grinding and slow cooling in a furnace. The obtained disk-shaped samples are well grounded again, then pelletized and sintered at 1400 °C for 24 h. Finally, the sintered ceramic samples are slowly cooled to room temperature in air. As the sample have been elaborated in air, it is consequently stoichiometric in oxygen. The composite sample is made by thoroughly mixing 48% : 52% (by weight) of
polycrystalline powders of La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ and La$_{1.3}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$ in an agate mortar for 30 min. The obtained compound will be referred as A$_{0.48}$/B$_{0.52}$. The samples are indexed with respect to Sr$_5$Ti$_3$O$_7$-type perovskite with I4/mmm space group. As a La-bilayer-structured perovskite, these compounds are generally formed of the bilayers MnO$_2$ (magnetic conducting layer) separated by a monolayer rock-salt-type (La, Ca)$_2$O$_3$ (non-magnetic insulating layer) along the c axis. Meanwhile, some small secondary phases attributed to the presence of CaO impurity with space group Fm$ar{3}$m and a fraction of with La$_{0.67}$Ca$_{0.33}$MnO$_3$ type orthorhombic structure with space group Pbmm are observed in both samples. Both impurities are identified with X’Pert HighScore Plus software. For both compounds, the positions of the La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ for A sample (La$_{1.4}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$ for B sample), La$_{0.67}$Ca$_{0.33}$MnO$_3$, and CaO peaks are denoted by the three sets of vertical bars (green color online), the top row corresponding to La$_{1.4}$Sr$_{1.6}$Mn$_2$O$_7$, La$_{1.3}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$, etc. The Rietveld refinement of the XRD data indicates that the replacement of 10% lanthanum with europium in the system does not affect the tetragonal structure but causes a decrease in the cellular parameters $a = b, c$ and the unit cell volume $V$. The lattice parameters of these compounds are found to be $a = 3.870 \, \AA$, $c = 19.302 \, \AA$ and $V = 289.059 \, \AA^3$ for La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ (A) and $a = 3.866 \, \AA$, $c = 19.281 \, \AA$ and $V = 288.219 \, \AA^3$ for La$_{1.3}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$ (B). The quality of the refinement is evaluated through the goodness of the fit indicator $\chi^2$, which is 1.32% for A sample and 1.43% for B sample. This confirms that the refinement is acceptable. The profile factor is found to be $R_p = 19.3\%$ (19.3\%), weighed profile factor $R_{wp} = 20.2\%$ (20.6\%) and Bragg $R$-factor $R_{Bragg} = 7.57\%$ (4.98\%) for A sample (for B sample). The amounts of all phases present in the sample are quantified simultaneously using the Rietveld method. The phase quantification procedure involves the identification of major and minor phases. Here, quantitative phase analysis obtained by Rietveld refinement shows that the La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ (La$_{1.3}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$) is the dominant phase, constituting 89.7\% (87.4\%) of the weight. The La$_{0.67}$Ca$_{0.33}$MnO$_3$ and the CaO phases account for only 6.1\% (7.9\%) and 4.2\% (4.7\%), respectively. The latter phase is frequently encountered after the final step of the synthesis of LaCa-bilayer manganites. Given the small concentration of the impurities, we assume that the secondary phase does not have any significant effect on the subsequent measurements of physical properties.

Fig. 2 depicts the temperature dependence of magnetization $M(T)$ for both A and B samples under an applied magnetic field of 0.05 T in field cooled mode (FC). It is clear from Fig. 2 that the $M(T)$ curves do not reveal secondary magnetic phases, which in turn suggests that the presence of small amount of impurities does not have any significant effect on the thermomagnetic properties. The $M(T)$ curves show rapid decrease of magnetization at Curie temperature which is the signature of the transition from ferromagnetic to paramagnetic state.

Furthermore, it can be seen from Fig. 2 that replacing La by Eu causes the value of $T_C$ to shift from 240 K for La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ (A) to 200 K for La$_{1.3}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$ (B). The Curie temperature $T_C$ is defined as the inflection point of $dM/dT$ (see inset Fig. 2). It is clear that the pristine compound La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ is ferromagnetic below $T_C = 240$ K. This value is higher than $T_C = 235$ K given by ref. 30 and smaller than $T_C = 270$ K observed in the same sample provided by ref. 31. This

![Fig. 1](image-url) The XRD patterns for A and B samples performed at room temperature. (a) La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ and (b) La$_{1.3}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$.
dissimilarity may be explained by the sensitivity of Curie temperature to the preparation conditions and the temperature of sintering which leads to the conclusion that the preparation processes have enormous impacts on the performance of magnetic materials.

Fig. 3(a) shows the magnetic hysteresis loops of both A and B samples taken at 10 K. Both loops show nearly zero coercivity, high magnetization saturation and negligible hysteresis which means that A and B bilayer manganites exhibit perfect magnetic reversibility or soft ferromagnetic nature. These observed outstanding soft-magnetic properties are beneficial for the application as bulk magnetic refrigerants. Furthermore, it can be seen that they display scarcely any hysteresis loss, although the two compounds exhibit the nature of first-order phase transition. This point is very attractive for magnetic refrigeration.

Isothermal magnetization \( M(\mu_0H) \) curves are performed around transition temperature for each sample. Fig. 3(b) and (c) represents the recorded \( M(\mu_0H) \) curves of samples A and B over a wide range of the magnetic field ranging from 0 T to 5 T. At temperatures above 270 K for A sample (250 K for B sample) \( M(\mu_0H) \) curves show a linear behaviour as expected in the paramagnetic state. Below 220 K for A sample (190 K for B sample) \( M(\mu_0H) \) curves show an expected rapid increase at field values less than 0.4 T followed by the tendency to saturation at higher fields, which indicate the existence of a ferromagnetic state in the samples.

However, it can be clearly seen that the magnetization initially increases gradually with increasing \( \mu_0H \) for temperatures between 220 and 270 K for A sample (190 and 250 K for B sample). A sudden change appears above a critical magnetic field followed by a rapid increase of magnetization thus exhibiting an ‘S’ shaped \( M(\mu_0H) \) plot. This is a signature of a metamagnetic behaviour observed in the both samples. The latter phenomenon indicates the possibility of a large magnetic entropy change around Curie temperature. This point is very enticing for magnetic refrigeration. Motivated by our previous result of a large magnetocaloric effect \( -\Delta S_M(T, \mu_0H) = 7.23 \, J \)
kg\(^{-1}\) K\(^{-1}\) at 5 T (ref. 27) observed in Pr\(_{0.8}K_{0.2}\)MnO\(_3\) sample which showed a similar metamagnetic behavior, we investigated the MCE in both aforementioned compounds.\(^{26}\)

In the present work, it is interesting to evaluate the magnetocaloric effect of the A and B compounds. For this reason, we used the isothermal magnetisations measured at discrete temperatures to determine the MCE for each compound. Using Maxwell relation and magnetization curves (\(M-\mu_0H\)) we obtained the value of magnetic entropy changes \(\Delta S_M(T, \mu_0H)\) as a function of temperature in the magnetic field range of 0 to 5 T for both A and B samples. Fig. 4(a) and (b) depicts the behaviour of \(\Delta S_M(T, \mu_0H)\) for both compounds. The negative sign of the \(\Delta S_M(T, \mu_0H)\) seen in the latter figures is referred as the normal MCE and confirms the ferromagnetic nature of these samples.\(^{34-36}\) As one can see, the aforementioned materials illustrate significant values of the magnetic entropy changes and show that the magnitudes of \(\Delta S_M\) increases with an increase in the applied magnetic field. For \(\mu_0H = 5\) T, the entropy change \(\Delta S_M\) exhibits a maximum value of 6.6 J kg\(^{-1}\) K\(^{-1}\) around \(T_{\text{peak}}\sim 245\) K for A sample (6.25 J kg\(^{-1}\) K\(^{-1}\) around \(T_{\text{peak}}\sim 215\) K for B sample) and it decreases on either side. However, the magnitude of \(\Delta S_M\) increases and the peak of \(\Delta S_M\) becomes asymmetrical with the rise of magnetic field. While \(\Delta S_M\) diminishes abruptly with lowering temperature below the peak, it gradually falls with the rise of temperature above the peak. We can also remark that \(\Delta S_M\) curves for the both samples present higher peak values and are quite similar in the temperature range of \(\Delta T = T_{\text{CA}} - T_{\text{CB}} \approx 40\) K. Due to the remarkable similarities in the results, the two materials provide an opportunity to manufacture a composite with high performance in the context of magnetic refrigeration.

In this context, magnetic properties for La\(_{1.4}Ca_{1.6}\)Mn\(_2\)O\(_7\) (A) and La\(_{1.3}Eu_{0.1}Ca_{1.6}\)Mn\(_2\)O\(_7\) (B) are described in more detail by means of simulation of \(\Delta S_M(T, \mu_0H = 5\) T) of individual compounds La\(_{1.4}Ca_{1.6}\)Mn\(_2\)O\(_7\) (A) and La\(_{1.3}Eu_{0.1}Ca_{1.6}\)Mn\(_2\)O\(_7\) (B) (see Fig. 5(a)). A numerical method is used to determine the optimum mass ratios of \(x\) refrigerant samples and the resulting
entropy change $\Delta S_M(T, \mu_dH = 5\, \text{T})$ of the composite.\cite{22} Fig. 5(b) illustrates the numerical calculations for $\Delta S_M(T, \mu_dH = 5\, \text{T})$ curves in the vicinity of the magnetic transition temperatures for the investigated materials and their composite. The $\Delta S_M(T, x)$ for $(\text{La}_{1.4}\text{Ca}_{1.6}\text{Mn}_2\text{O}_7)_{1-x}/(\text{La}_{1.3}\text{Eu}_{0.1}\text{Ca}_{1.6}\text{Mn}_2\text{O}_7)$ composites produced by combining a $1 \times (\text{La}_{1.4}\text{Ca}_{1.6}\text{Mn}_2\text{O}_7)$ and a $x \times (\text{La}_{1.3}\text{Eu}_{0.1}\text{Ca}_{1.6}\text{Mn}_2\text{O}_7)$ were obtained from their respective $\Delta S_M(T)$ according to the following equation:

$$\Delta S_M(T, x) = [(1 - x) \Delta S_{M,A}(T) + x \Delta S_{M,B}(T)]$$

(1)

where $x$ ($0 \leq x \leq 1$) represents the relative weight fraction between A and B compounds. The last equation is used to estimate the $|\Delta S_M(T, x)|$ because it has been demonstrated that the component phases in the solid magnetic refrigerants are mixed without any interactions among themselves; therefore it does not affect the resultant $|\Delta S_M(T, x)|$.\cite{23} It is clear from Fig. 5(b) that the numerical $\Delta S_M(T, x)$ represent a double peak resulting from the difference between Curie temperatures $\Delta T_C = T_{CA} - T_{CB}$ of the constitutive phases for certain values of $x$. We can also see in the same figure that the magnetocaloric responses show a broad single peak for other values of $x$ which is clearly obvious near the extreme values $x = 0$ or $x = 1$. The remarkable feature in Fig. 5(b) is that the central region of $\Delta S_M(T, x)$ becomes relatively flat for $x = 0.48$ which shows a table-like behaviour.

To explore the performance of this composite, we have calculated the refrigerant capacity (RC) which is another decisive parameter for evaluating and approving cooling efficiency.\cite{24,25} The RC parameter measures the amount of heat convey between the cold and hot reservoirs in the thermodynamic cycle. Thus, it has been suggested as a more suitable indicator of magnetic substances utility for solid-state refrigeration. For practical cooling systems, the RC with a broad temperature range is suitable for the active magnetic refrigeration cycle.\cite{26,27,28}

The refrigerant capacity depends not only on the maximum of $\Delta S_M(T)$, but also on the overall profile of $\Delta S_M(T)$. RC is obtained by numerical integration of the area under the $\Delta S_M(T)$ curve. The limits of the temperature integration are set by the half-maximum of the $\Delta S_M(T)$ peak, where $T_{\text{Hot}}$ and $T_{\text{Cold}}$ correspond to the two temperatures at which the $|\Delta S_M(T)|$ value is half of the peak value.\cite{29}

$$\text{RC} = \left| \int_{T_{\text{Cold}}}^{T_{\text{Hot}}} \Delta S_M(T) dT \right|$$

(2)

Accordingly, we report a detailed investigation of the MCE response as a function of the composite ratio; we present in Fig. 6(a) the $x$ dependence of $\Delta S_M^{\text{Max}}, \Delta T_{\text{FWHM}}$ and the RC values for the composite system $A_xB_{1-x}$ at $\mu_dH = 5\, \text{T}$. This figure confirms that the important value of $\Delta T_{\text{FWHM}}$ correspond to $x = 0.48$. The existence of the table-like behaviour could give rise to the maximum values of $\Delta T_{\text{FWHM}}$ and RC, which allows the $A_{0.48}/B_{0.52}$ composite to become a promising compound for different thermodynamic cycles used in magnetic cooling technology.

Based on these calculations and in order to produce a composite with table-like MCE for a magnetic cooling system using the Ericsson thermodynamic cycle, powdered specimen of the $(\text{La}_{1.4}\text{Ca}_{1.6}\text{Mn}_2\text{O}_7)_{1-x}/(\text{La}_{1.3}\text{Eu}_{0.1}\text{Ca}_{1.6}\text{Mn}_2\text{O}_7)$ composite is made by repetitive grinding and mixing of the two compositions in the desired ratio of $48-52\%$ ($A_{0.48}/B_{0.52}$). After preparing the composite, the temperature ($T$) dependence of the magnetization ($M$) is measured in field-cooled mode (FC) under an applied field of $0.05\, \text{T}$. The results are depicted in Fig. 6(b) for our new compound. This curve clearly shows that the investigated composite specimen exhibits two magnetic transitions because of its heterogeneous composition. It is also observed in Fig. 6(b) that the pronounced two minima in the $dM/dT \text{versus} \, T$ curve confirm that the composite contains two magnetic phase transitions compared with individual A and B bilayer manganites. The later successive minima correspond exactly to $T_C$ for each of the constituent phases A and B used to prepare the $A_{0.48}/B_{0.52}$ composite. It is worthwhile to mention that the magnetization magnitude of the studied composite shows a small decrease at low temperatures as compared with that of A and B bilayer manganites. The existence of two transition temperatures.
originating from different phases can certainly have an important effect on the MCE characteristics because the shape and behaviour of the magnetic entropy change are highly sensitive to the character of the magnetic phase transition.

It is demonstrated that the presence of two magnetic phases in the refrigerant material ensure that the material has a large MCE with a broad refrigeration temperature range and enhanced RC. In this investigation, we used the presence of two magnetic transitions to confirm our above calculation and for generating a broad range of MCE with a significant increase in RC.

To get deeper insight into the magnetocaloric response of the prepared composite upon changing the magnetic field from 0 to 5 T, isothermal magnetization curves of A0.48/B0.52 are measured as a function of the applied field recorded at different temperatures.

The measured $M(\mu_0 H)$ plots are shown in Fig. 7(a). In Fig. 7(b) we compare the selected isothermal $M-\mu_0 H$ curves plotted with applied fields between 0 and 5 T at $T = 10$, $220$, $250$ and $320$ K for the individual samples and the A0.48/B0.52 composite. It is observed from this figure that the A0.48/B0.52 sample has similar values of magnetization at 10 K and 320 K as compared to A and B samples. In addition, the $M(\mu_0 H)$ curves are typical for a ferromagnetic state at 10 K and for a paramagnetic state at 320 K. On the other side, at 220 K and 250 K, the three compounds present different shapes in $M(\mu_0 H)$ and the composite system shows the intermediate values of magnetization compared to that of the constituent phases A and B. In this temperature range, the slightly jump in the $M(\mu_0 H)$ curves may be attributed to strong domain wall pinning in the ferromagnetic state.

The temperature dependences of magnetic entropy changes, $-\Delta S_M(T)$, taken at 1, 2, 3, 4 and 5 T for the A0.48/B0.52 composite is presented in Fig. 8(a). All the curves of $-\Delta S_M(T)$ have a clear double-peak shape (two $\Delta S_M$ values), resulting from the disparity in Curie temperature of both phases A and B. The latter double-peak shape is very noticeable at low $\mu_0 H$ and

Fig. 7  (a) Isothermal magnetization curves at various temperatures for the composite and (b) $M(\mu_0 H)$ at 10, 220, 250 and 320 for all samples.

Fig. 8  (a) Magnetic entropy change, $\Delta S_M$ vs. temperature for the composite system and (b) comparison between experimental and simulation.
begins to flatten gradually in favor of the table-like behaviour occurring at higher magnetic fields. This behaviour could give rise to the maximum values of $\Delta T_{\text{FWHM}}$ and the RC refrigerant capacity strongly required for the ideal Ericsson cycle magnetic refrigeration over a broad temperature range.\textsuperscript{41}

Fig. 8(b) depicts experimental and theoretical entropy change curves for $\mu_0 H = 5 \text{T}$ of phases A and B that make up the composite with $T_{\text{C,A}} = 200 \text{ K}$ and $T_{\text{C,B}} = 240 \text{ K}$, along with $\Delta S_{\text{M}}(T)$ in the composite $x = 0.48$. Latest figure demonstrates that the agreement between the experimental curves $\Delta S_{\text{M}}(T)$ and that predicted by eqn (1) is excellent. According to this agreement, we can conclude that the numerical calculations are valid in the choice of MCE composite and can thus be used as means of designing magnetic refrigerant materials with an improved magnetocaloric response for the desired magnetic fields. The maximum value of $-\Delta S_{\text{M}}(T)$ is found to be 4.07 J kg$^{-1}$ K$^{-1}$ for $A_{0.48}/B_{0.52}$ in a wide temperature range. The magnitude of $-\Delta S_{\text{M}}(T)$ is reduced in the $A_{0.48}/B_{0.52}$ composite which gives a broad table-like behaviour with a wide temperature range compared to that of the pure constituent phases. Basically, in an ideal Ericsson cycle, the entropy conveyed between two heat reservoirs ($T_{\text{Hot}}$ and $T_{\text{Cold}}$) should be as constant as possible to avoid the generation of irreversible work.\textsuperscript{42} For this reason, the flattening of $-\Delta S_{\text{M}}(T, x = 0.48)$ curve can be able to meet the latter requirements for the use of $A_{0.48}/B_{0.52}$ as a composite for Ericsson-cycle-based magnetic refrigerators.\textsuperscript{43}

From eqn (2), the obtained value of RC is $\sim 205.92 \text{ J kg}^{-1}$ at 5 T in B sample while it does not exceed $\sim 178.92 \text{ J kg}^{-1}$ in A sample which indicate that the Eu-substitution increase the refrigerant capacity. Fig. 9(a) shows $\Delta S_{\text{M}, \text{max}}$, $\Delta T_{\text{FWHM}}$ and RC plots as a function of the applied magnetic field. As displayed in Fig. 9(b), the obtained values of $\Delta S_{\text{M}, \text{max}}$, $\Delta T_{\text{FWHM}}$ and RC are strongly related to the magnetic field. It is clearly observed that the A material has smaller values of $\Delta T_{\text{FWHM}}$ than the B sample. Compared to gadolinium, which is considered as the typical ferromagnetic material for magnetic refrigeration, the RC values of the A and the B samples represents about $\sim 56.13\%$ and $\sim 64.6\%$ of the RC estimated for Gd (the value of RC is around 25% lower than that of the relative refrigerant capacity RCP for the $\Delta S_{\text{M}}(T)$\textsuperscript{44} from ref. 45 RCP Gd = 425 J kg$^{-1}$ then RC Gd = $\frac{1}{2}$ $\times$ RCP Gd = $\frac{1}{2}$ $\times$ 425 $\sim$ 319 J kg$^{-1}$). According to the obtained result, the Eu-doped sample is still valuable for magnetic refrigeration at low temperatures. These values are much larger than that of several manganites\textsuperscript{46,47} and are high enough for magnetic cooling. Refrigerants with high working temperatures and high RC are in fact very beneficial to magnetic cooling applications\textsuperscript{48} and suggests that compounds can thus be used as an active magnetic refrigeration materials suggested by Barclay.\textsuperscript{49} However, in this case the maximum values of $\Delta T_{\text{FWHM}}$ for all three samples A, B and $A_{0.48}/B_{0.52}$ are equal to $\sim 35.7 \text{ K}$, $\sim 41.54 \text{ K}$ and $\sim 68.16 \text{ K}$ respectively for a field of 5 T. It can be observed that the highest value of $\Delta T_{\text{FWHM}}$ is revealed for the $A_{0.48}/B_{0.52}$ composite and an increment of $\sim 47.63\%$ and $\sim 39.05\%$ in $\Delta T_{\text{FWHM}}$ compared with the individual $La_1.4Ca_{1.6}Mn_2O_7$ and $La_1.3Eu_{0.1}Ca_{1.6}Mn_2O_7$ samples are observed. This enhancement in $\Delta T_{\text{FWHM}}$ is an outcome of the augmentation of RC despite the diminution of the maximum value of $\Delta S_{\text{M}}$.

However, it follows that a compromise is necessary between the value of the $\Delta T_{\text{FWHM}}$ and the energy losses and the efficiency of machine (due to an increase of cycles in the heat exchange medium). The investigated $A_{0.48}/B_{0.52}$ composite exhibit nearly constant value of $\Delta S_{\text{M}}(T)$ with width of $\sim 68.16 \text{ K}$. The present results confirm that the field and the temperature range used in the numerical calculation are analogous to those explored experimentally and ensure that the large $\Delta T_{\text{FWHM}}$ observed in the prepared composite have a great importance for cooling capacity.

The broadening width of $\Delta S_{\text{M}}(T)$ is expected to make an increase of RC in the composite as predicted by eqn (2). In this study, it should be noted that the used $T_{\text{Cold}}$ and $T_{\text{Hot}}$ are defined as temperatures fulfilling $\Delta S_{\text{M}}(T_{\text{Cold}}) = \Delta S_{\text{M}}(T_{\text{Hot}}) = \Delta S_{\text{M}, \text{max}}/2$. In order to visualize RC ($T_{\text{Cold}}$) and obtain the RC values at different values of $T_{\text{Cold}}$, the integrand is evaluated from high temperature ($T_{\text{Hot}}$) to low temperature ($T_{\text{Cold}}$) as depicted in eqn (2). Fig. 9(b) shows the calculated values of RC as a function of $T_{\text{Cold}}$ under 5 T magnetic field of A, B and $A_{0.48}/B_{0.52}$ compounds. It is found that the RC increases as $T_{\text{Cold}}$ is separate from the $\Delta S_{\text{M}}$ peak temperature ($T_{\text{peak}}$), at which RC is
zero due to eqn (2). In the temperature span of \( T_{\text{Hot}} - T_{\text{Cold}} = \Delta T_{\text{FWHM}} \), the estimated RC values correspond to A, B and \( A_{0.48}B_{0.52} \) samples are 178.92 J kg\(^{-1}\), 205.92 J kg\(^{-1}\) and 232.85 J kg\(^{-1}\)

respectively. These values show that the RC of the composite \( A_{0.48}B_{0.52} \) is improved by 23.16% and 11.56% when compared with those of A and B samples. This proves the superior cooling power of the \( A_{0.48}B_{0.52} \) sample and refers to a possible way to optimize RC of refrigerant magnetic materials. This result reveals that the \( A_{0.48}B_{0.52} \) is a promising compound to be used as a refrigerant material in solid-state refrigeration with the Ericsson cycle. Similar reinforcement in RC responses are observed in many composite systems like \( \text{La}_{1.4}\text{Ca}_{1.6}\text{Mn}_{2}\text{O}_{7}/\text{La}_{0.7}\text{Ca}_{0.3}\text{Mn}_{18}\text{O}_{39} \), \( \text{FeZrB(Cu)} \), and \( \text{La}_{0.5}\text{Ca}_{0.1}\text{Mn}_{18}\text{O}_{39}/\text{La}_{0.5}\text{Ca}_{0.3}\text{Mn}_{18}\text{O}_{39} \).

To make our analysis more complete, we are concerned with the nature of the magnetic phase transition in our bilayer manganites. For that reason, we have investigated the field dependence of MCE in A, B and \( A_{0.48}B_{0.52} \) samples by using the relation expressed as \( \Delta S_M \approx a(\mu_0H)^N \). The latter relationship makes it possible to determine the nature of the magnetic phase transition observed in the aforementioned samples. Recently, J. Y. Law et al. proposed a quantitative criterion to identify the order of magnetic phase transitions using the field dependence of magnetocaloric effect. For materials with the first-order magnetic phase transition (FOPT), \( \Delta S_M \) depends on the field with exponent \( N > 2 \). Particularly, for magnetic samples, the local exponent \( N(T,\mu_0H) \) can be calculated from the logarithmic derivative of the experimental \( \Delta S_M(T, H) \):

\[
N(T, \mu_0H) = \frac{d \ln(-\Delta S_M(T, \mu_0H))}{d \ln(\mu_0H)}
\]

The temperature dependence of \( N \) is illustrated in Fig. 10(a) for A, B and \( A_{0.48}B_{0.52} \) samples. The exponent \( N \) for A and B samples has a minimum value at \( T_c \). However, for \( A_{0.48}B_{0.52} \), the \( N(T) \) curves exhibits two minima whose positions are related to the critical temperatures of the existing phases (A and B) in this composite. On the one hand, it is observed in Fig. 10 that the exponent \( N \) is sensitive to the magnetic field in the entire studied temperature range and the magnetic entropy changes, \( \Delta S_M \). The value of \( N(T_c) \) has 0.4 at high magnetic fields indicates that our samples undergo first order magnetic transition temperature. In the other hand and under critical temperatures, the \( N(T) \) curves increase gradually with the temperature drop and approaches 1 for higher magnetic fields. Far above \( T_c \), the \( N(T) \) values overshoots 2 (\( N > 2 \)) in the paramagnetic region (near magnetic transitions) of all three samples. This overshoot is more pronounced in sample B compared to sample A and the composite \( A_{0.48}B_{0.52} \). The observed behaviour shows that the quantitative criterion of \( N > 2 \) near the transition is valid for monophase and biphasic materials which indicates that our samples exhibit a first-order transition. This is in agreement with the previous observations in \( N(T_c) \) values. A similar behaviour is reported in other magnetic materials with first-order transition. However, the order of magnetic phase transition is usually revealed by the Arrott plots \( (M^2 \text{ vs. } H/M) \). For more confirmation of the nature of the magnetic phase transition of A, B and \( A_{0.48}B_{0.52} \) samples, the curves of \( M^2 \text{ vs. } H/M \) plotted at different temperatures are exhibited in Fig. 11. The Arrott plots for the aforementioned materials just above the respective \( T_c \) are displayed in the inset of the Fig. 11. According to the Banerjee criterion, the obviously negative slopes of Arrott plots verify the first-order nature of the three samples, which is consistent with the quantitative criterion.
4. Conclusion

In summary, we have first investigated the structural, magnetic and magnetocaloric properties of La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ and La$_{1.3}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$ samples prepared by the standard solid-state reaction method. The magnetic study showed that our investigated samples exhibit a PM–FM transition and present large magnetocaloric properties. Secondly, we have prepared a composite using the aforementioned samples with weight ratio of 48–52%. The latter ratio is determined numerically to obtained high magnetocaloric performances. Compared with the main polycrystalline phases, the magnetic entropy change of the prepared composite was found to be smaller. The prepared composite is characterized by important values of $\Delta T_{\text{FWHM}}$ (68.16 K under 5 T) and RC (232.85 J kg$^{-1}$ under 5 T). The refrigeration capacity of the composite is enhanced by 23.16% and 11.56% when compared with those of the individual La$_{1.4}$Ca$_{1.6}$Mn$_2$O$_7$ and La$_{1.3}$Eu$_{0.1}$Ca$_{1.6}$Mn$_2$O$_7$ samples. Hence, the results of the $A_{0.48}/B_{0.52}$ composite represent a significant motivation to search for new suitable magnetic material with several reversible magnetic transitions originating from two different phases in order to expand working temperature with the same sign of successive magnetic entropy changes. These observations corroborate that the magnetic refrigerant compound with the more competitive characteristics may be developed in a form of a composite material that can lead to a future cheaper, more efficient and green refrigerator. In addition, our magnetocaloric investigation shows that the first order phase transition is observed on our compounds. We showed that using the field dependence of magnetocaloric effect, the order of the phase transition can be unambiguously determined using a quantitative criterion even for $N > 2$ near the transition of monophasic and biphasic magnetocaloric materials. The order of the magnetic phase transition of the three samples is corroborate by using the Banerjee criterion.

Conflicts of interest

There are no conflicts of interest to declare.

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