MPC-Based Emergency Vehicle-Centered Multi-Intersection Traffic Control

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Abstract—This article proposes a traffic control scheme to alleviate traffic congestion in a network of interconnected signaled lanes/roads. The proposed scheme is emergency vehicle-centered, meaning that it provides an efficient and timely routing for emergency vehicles. In the proposed scheme, model predictive control is utilized to control inlet traffic flows by means of network gates, as well as the configuration of traffic lights across the network. Two schemes are considered in this article: 1) centralized and 2) decentralized. In the centralized scheme, a central unit controls the entire network. This scheme provides the optimal solution even though it might not fulfill real-time computation requirements for large networks. In the decentralized scheme, each intersection has its own control unit, which sends local information to an aggregator. The main responsibility of this aggregator is to receive local information from all control units across the network and the emergency vehicle, augment the received information, and share it with the control units. Since the decision-making in a decentralized scheme is local and the aggregator should fulfill the abovementioned tasks during a traffic cycle, which takes a long period of time, the decentralized scheme is suitable for large networks even though it may provide a suboptimal solution. Extensive simulation studies are carried out to validate the proposed schemes and assess their performance. Notably, the obtained results reveal that traveling times of emergency vehicles can be reduced up to ~50% by using the centralized scheme and up to ~30% by using the decentralized scheme without causing congestion in other lanes.

Index Terms—Centralized control, decentralized control, emergency vehicle, model predictive control (MPC), multi-intersection control, traffic control.

I. INTRODUCTION

Traffic congestion is one of the most critical issues in urbanization. In particular, many cities around the world have experienced a 46%–70% increase in traffic congestion [1]. Congested roads not only lead to increased commute times but also hinder timely deployment of emergency vehicles [2]. Hence, emergency vehicles often fail to meet their target response time [3]. According to ~240 million emergency calls every year in the U.S. [4], such hindering greatly affects hospitalization and mortality rates [5].

The common practice by regular vehicles (i.e., nonemergency vehicles) in the presence of an emergency vehicle is to pull over to the right (in two-way roads) or to the nearest shoulder (in one-way roads) [6], and let the emergency vehicle traverse efficiently and timely. This is not always possible, as, in dense areas, the edges of the roads are usually occupied by parked/moving vehicles.

The chance of an emergency vehicle getting stuck is even higher when it has to traverse intersections with cross-traffic [7]. Note that the majority of incidents involving emergency vehicles happen within intersections [8]. One possible way to cope with this problem is to use traffic lights at intersections to detect emergency vehicles and facilitate their fast and efficient travel. For this purpose, traffic lights in most parts of the U.S. are equipped with proper detectors (e.g., 3M Opticom [9]), and emergency vehicles are equipped with emitters that broadcast an infrared signal. When the receiver on a traffic light detects a recognized signal, the traffic light changes to allow priority access to the emergency vehicle.

In this context, the “green wave” method has been proposed to reduce emergency vehicles’ traveling time [10]. In the “green wave” method, a series of traffic lights are successively set to “green” to allow the timely passage of emergency vehicles through several intersections [11]. The main issue with the “green wave” method is that it leads to prolonged red lights for other lanes [12], meaning that it may cause congestion in other lanes.

A different method for controlling the traffic in the presence of an emergency vehicle is to convert the traffic control problem to a real-time scheduling problem [3], [13]. The core idea of this method is to model the vehicles and traffic lights as aperiodic tasks and sporadic servers, respectively, and then to utilize available task scheduling schemes to solve the resulting problem. Other existing traffic control methods either do not consider emergency vehicles [14]–[19] or require vehicle to vehicle connectivity [20]–[25]. Note that the presence of 100% of connected vehicles is not expected until 2050 [26], making these methods inapplicable to the current traffic systems.

The aim of this article is to propose control algorithms to manipulate traffic density in a network of interconnected...
signaled lanes. The core idea is to integrate the cell transmission model (CTM) [27], [28] with model predictive control (MPC) [29]. Our motivation to use MPC is that it solves an optimal control problem over a receding time window, which provides the capability of predicting future events and taking actions accordingly. Note that, even though this approach is only suboptimal, in general [30], it works very well in many applications; our numerical experiments suggest that MPC yields very good performance in traffic control applications. Two schemes are developed in this article: 1) centralized and 2) decentralized. In the centralized scheme, assuming that the control inputs are inlet traffic flows and the configuration of the traffic lights across the network, a two-step control scheme is proposed. In a normal traffic mode, the proposed centralized scheme alleviates traffic density in all lanes, ensuring that traffic density in the entire network is less than a certain value. When an emergency vehicle approaches the network—this condition is referred to as an emergency traffic mode—the control objective is to clear the path for the emergency vehicle without causing congestion in other lanes. It is shown that our proposed centralized scheme provides the optimal solution even though its computation time (CT) may be large for large networks. In the decentralized scheme, inlet traffic flows and the configuration of the traffic lights at each intersection are controlled by a local control unit, while the control units share data with each other through an aggregator. In the decentralized scheme, the aggregator should receive and send the data during every traffic light state (i.e., “red” or “green”). Since the traffic cycle ranges from 1 to 3 min in real-world traffic systems [31], the smallest duration of traffic light states is 30 s; thus, the maximum allowable communication delay is around 30 s, which is achievable even with cheap communication technologies. Thus, the decentralized scheme is more suitable for large networks even though it yields a suboptimal solution. Note that the robustness and tolerance of the decentralized scheme to uncertainty in communication delay and communication failures are out of the scope of this article and will be considered for future work.

The key contributions of this article are: 1) we develop a traffic control framework, which provides an efficient and timely emergency vehicle passage through multiple intersections, without causing congestion in other lanes; 2) we propose a centralized scheme for small networks and a decentralized scheme for large networks that address scalability issues in integrating CTM and MPC; and 3) we validate our schemes via extensive simulation studies and assess their performance in different scenarios. The main features of the proposed framework are: 1) it is general and can be applied to any network of interconnected signaled lanes and 2) it does not require vehicle-to-everything (V2X) connectivity, and hence, it can be utilized in the currently existing traffic systems; the only communication requirement is between the emergency vehicle and the central control unit in the centralized scheme and with the aggregator in the decentralized scheme. Note that this article considers only macroscopic characteristics of traffic flow; it is evident that the existence of V2X connectivity can not only be exploited to further improve efficiency at the macrolevel, but it can also be leveraged to ensure safety and avoid collisions.

The key innovations of this article with respect to prior work are: 1) formulating the traffic density control problem in both normal and emergency modes as MPC problems; 2) developing a two-step optimization procedure implementable in the current traffic systems; and 3) deriving centralized and decentralized schemes for traffic networks with different sizes and communication capacities.

The rest of this article is organized as follows. Section II describes the macroscopic discrete-time model of the traffic flow in the network. Section III discusses the design procedure of the centralized traffic control scheme. The decentralized scheme is discussed in Section IV. Section V reports simulations results and compares the centralized and decentralized schemes. Finally, Section VI concludes this article.

A. Notations

$\mathbb{R}$ denotes the set of real numbers, $\mathbb{R}_{\geq 0}$ denotes the set of nonnegative real numbers, $\mathbb{Z}$ denotes the set of integer numbers, and $\mathbb{Z}_{\geq 0}$ denotes the set of nonnegative integer numbers. For the matrix $X$, $X^\top$ denotes its transpose, $\rho(X)$ denotes its spectral radius, and $\|X\|_1 = \sup_{y \neq 0}(\|XY\|_1)/\|y\|_1$ with $\|\cdot\|_1$ as the $\ell_1$-norm. For the vector $y$, $|y|_\infty$ is the elementwise rounding to the closest nonnegative integer function. For given sets $X, Y, X \oplus Y = \{x + y : x \in X, y \in Y\}$ is the Minkowski set sum. Table I lists the essential notation of this article.

### II. System Modeling

In this section, we formulate the traffic control problem for a general traffic network.

#### A. Traffic Network

Consider a traffic network with $N$ lanes and $M$ intersections. There are $N_{\text{in}} < N$ inlets through which vehicles enter the

| Type       | Symbol | Description                                                                 |
|------------|--------|-----------------------------------------------------------------------------|
| Calligraphic | $\mathcal{N}$ | Set of lanes                                                                |
|            | $\mathcal{M}$ | Set of intersections                                                        |
|            | $\mathcal{G}$ | Traffic network                                                             |
|            | $\mathcal{E}$ | Edge of traffic graph                                                       |
|            | $\mathcal{X}$ | Constraint set                                                              |
|            | $\mathcal{D}$ | Disturbance set                                                             |
| Greek      | $\Lambda$ | Set of possible commands by traffic lights                                  |
|            | $\lambda$ | Configuration of traffic lights                                             |
|            | $\gamma$ | Prioritizing parameter                                                      |
| Latin      | $x$    | Traffic density                                                             |
|            | $y$    | Traffic inflow                                                              |
|            | $z$    | Traffic outflow                                                             |
|            | $u$    | Inlet flow                                                                  |
|            | $d$    | Disturbance input                                                           |
|            | $t$    | Discrete time instant                                                       |
|            | $k$    | Prediction time instant                                                     |
| Subscript and Superscript | $in$ | Inlet                                                                       |
|            | $df$ | Disturbance-free                                                            |
|            | $\text{nom}$ | Nominal                                                                     |
|            | $n$    | Normal condition                                                           |
|            | $e$    | Emergency condition                                                         |
|            | $t$    | Computed at time $t$                                                        |

| TABLE I | LIST OF CALLIGRAPHIC, GREEK, LATIN, AND SUBSCRIPT AND SUPERSCRIPT SYMBOLS |
network. We denote the set of lanes by \( N = \{1, \ldots, N\} \), the set of intersections by \( M = \{1, \ldots, M\} \), and the set of inlets by \( N_{in} \subset N \).

The considered traffic network can be represented by a graph \( G(N, E) \), where \( E \subset N \times N \) defines the edge of graph. The edge \((i, j) \in E\) represents a directed connection from lane \( i \) to lane \( j \). Since all lanes are assumed to be unidirectional (note that two-way roads are modeled as two opposite-directional lanes), if \((i, j) \in E\), we have \((j, i) \not\in E\). Also, we assume that U-turns are not allowed, i.e., \((i, j), (j, i) \not\in E\), if lanes \( i \) and \( j \) are opposite-directional lanes on a single road.

Note that we assume that the traffic graph \( G(N, E) \) remains unchanged, that is, we do not consider graph changes due to unexpected events (e.g., changes in the edge \( E \) as a result of lane blockages due to accidents). We leave the developments of strategies for rerouting in the case of a change in the traffic graph to future work.

### B. Action Space by Traffic Lights

Suppose that all lanes, except outlets, are controlled by traffic lights that have three states: “red,” “yellow,” and “green.” The vehicles are allowed to move when the light is “yellow” or “green,” while they have to stop when the light is “red.” This means that there are practically two states for each traffic light.

Let \( \lambda_j(t) \) be the configuration of traffic lights at intersection \( j \in M \) at time \( t \). We denote the set of all possible configurations at intersection \( j \) by \( \Lambda_j = \{\lambda_j, 1, \ldots, \lambda_j, \mu_j\} \), where \( \mu_j \in \mathbb{Z}_{\geq 0} \). Indeed, the set \( \Lambda_j \) represents the set of all possible actions that can be commanded by the traffic lights at intersection \( j \). Therefore, the set of all possible actions by traffic lights across the network is \( \Lambda = \Lambda_1 \times \cdots \times \Lambda_M \), and the \( M \)-tuple \( \lambda(t) = (\lambda_1(t), \ldots, \lambda_M(t)) \in \Lambda \) indicates the action across the network at time \( t \).

### C. Macroscopic Traffic Flow Model

The traffic density in each lane is a macroscopic characteristic of traffic flow [32], [33], which can be described by the CTM that transforms the partial differential equations of the macroscopic Lighthill–Whitham–Richards (LWR) model [34] into simpler difference equations at the cell level. The CTM formulates the relationship between the key traffic flow parameters and can be cast in a discrete-time state-space form.

Let the traffic density be defined as the total number of vehicles in a lane at any time instant; then, the traffic inflow is defined as the total number of vehicles entering a lane during a given time period, and the traffic outflow is defined as the total number of vehicles leaving a lane during a given time period. We use \( x_i(t) \in \mathbb{Z}_{\geq 0} \), \( y_i(t) \in \mathbb{R}_{\geq 0} \), and \( z_i(t) \in \mathbb{R}_{\geq 0} \) to denote the traffic density, the traffic inflow, and the traffic outflow in lane \( i \) at time \( t \), respectively. The traffic dynamics [35], [36] in lane \( i \) can be expressed as

\[
x_i(t+1) = [x_i(t) + y_i(t) - z_i(t)]_r, \tag{1}
\]

where the time interval \([t, t+1]\) is equivalent to \( \Delta T \) seconds. Since \( x_i(t) \) is defined as the number of existing vehicles in each lane, we use the rounding function in (1) to ensure that \( x_i(t) \) remains a nonnegative integer at all times. Given \( \Delta T \), \( y_i(t) \) and \( z_i(t) \) are equal to the number of vehicles entering and leaving the lane \( i \) in \( \Delta T \) seconds, respectively.

The traffic outflow \( z_i(t) \) can be computed as [19]

\[
z_i(t) = p_i(\lambda(t))x_i(t) \tag{2}
\]

where \( p_i(\lambda(t)) \) is the fraction of outflow vehicles in lane \( i \) during the time interval \([t, t+1]\), satisfying

\[
p_i(\lambda(t)) = \begin{cases} 0, & \text{if traffic light of lane } i \text{ is "red"} \\ \in [0, 1], & \text{if traffic light of lane } i \text{ is "green."} \end{cases} \tag{3}
\]

In other words, \( p_i(\lambda(t)) \) is the ratio of vehicles leaving lane \( i \) during the time interval \([t, t+1]\) to the total number of vehicles in lane \( i \) at time instant \( t \). It is noteworthy that, even though the impact of lane blockage or an accident in lane \( i \) can be modeled by adjusting \( p_i(\lambda(t)) \), this article does not aim to deal with such unexpected events.

**Remark 1:** We assume that outlet traffic flows are uncontrolled, i.e., there is no traffic light or gate at the end of outlets. This assumption is plausible, as any road connecting the considered traffic network to the rest of the grid can be divided at a macrolevel into an uncontrollable outlet inside the considered network and a lane outside the considered network (possibly controlled with a traffic light or a network gate). The extension of the proposed methods to deal with controlled outlet flows is straightforward by modifying (2) and all presented optimization problems to account for outlet flow (similar to what we do for inlet flow \( u_i(t) \)); thus, to simplify the exposition and subsequent developments, we will not discuss controlled outlets.

The traffic inflow \( y_i(t) \) can be computed as

\[
y_i(t) = \begin{cases} u_i(t), & \text{if } i \in N_{in} \\ \sum_{j=1}^{N} q_{ji}(\lambda(t))z_j(t), & \text{otherwise} \end{cases} \tag{4}
\]

where \( u_i(t) \in \mathbb{Z}_{\geq 0} \) is the inlet flow that is defined as the number of vehicles entering the traffic network through inlet \( i \) during the time interval \([t, t+1]\). The computed optimal inflows can be implemented by means of network gates, i.e., ramp meters [37], [38] for highways and metering gates [39] for urban streets. In (4), \( q_{ji}(\lambda(t)) \) is the fraction of outflow of lane \( j \) directed toward lane \( i \) during the time interval \([t, t+1]\), which is

\[
q_{ji}(\lambda(t)) = \begin{cases} 0, & \text{(if traffic light of lane } i \text{ is "red")} \\ \text{OR (if } (j, i) \not\in E) \\ \in [0, 1], & \text{(if traffic light of lane } i \text{ is "green")} \\ \text{AND (if } (j, i) \in E) \end{cases} \tag{5}
\]

and satisfies \( \sum_{i=1}^{N} q_{ji}(\lambda(t)) = 1 \) for all \( j \in N \). More precisely, \( q_{ji}(\lambda(t)) \) is the ratio of vehicles leaving lane \( j \) and entering lane \( i \) during the time interval \([t, t+1]\) to the total number of vehicles leaving lane \( j \) during the time interval \([t, t+1]\).
From (1) to (5), traffic dynamics of the entire network can be expressed as
\[ x(t + 1) = [\bar{A}(\bar{\lambda}(t))x(t) + B\bar{U}(t)]_+ \] (6)
where \( x(t) = [x_1(t) \cdots x_N(t)]^T \in \mathbb{Z}^N_{\geq 0} \), \( \bar{A} : \Lambda \to \mathbb{R}^{N \times N} \) is the so-called traffic tendency matrix \cite{Hoseinzadeh2020}, \( B \in \mathbb{R}^{N \times N_a} \), and \( \bar{U}(t) \in \mathbb{Z}^{N_{a}}_{\geq 0} \) is the boundary inflow vector. It should be noted that the \((i, j)\) element of \( B \) is 1 if lane \( i \) is the \( j \)th inlet and 0 otherwise.

**Remark 2:** At any \( t \), the \((i, i)\) element of the traffic tendency matrix \( \bar{A}(\bar{\lambda}(t)) = 1 - p_i(\bar{\lambda}(t)) \). Also, its \((i, j)\) element \((i \neq j) = q_{ij}(\bar{\lambda}(t))p_j(\bar{\lambda}(t)) \). As a result, since \( \sum_{i=1}^{N} q_{ij}(\bar{\lambda}(t)) = 1 \forall j \in N \), the maximum absolute column sum of the traffic tendency matrix is less than or equal to 1. This means that, at any \( t \), we have \( \|\bar{A}(\bar{\lambda}(t))\|_{1} \leq 1 \), which implies that \( \rho(\bar{A}(\bar{\lambda}(t))) \leq 1 \). Therefore, \( \rho(\bar{A}(\bar{\lambda}(t))\bar{A}(\bar{\lambda}(t + 1))\bar{A}(\bar{\lambda}(t + 2)) \cdots) \leq 1 \), which means that the unforced system (i.e., when \( \bar{U}(t) = 0 \)) is stable, although trajectories may not asymptotically converge to the origin. This conclusion is consistent with the observation that, in the absence of new vehicles entering to lane \( i \), the traffic density in lane \( i \) remains unchanged if the corresponding traffic light remains “red.”

**Remark 3:** In general, system (6) is not bounded-input-bounded-output stable. For instance, the traffic density in lane \( i \) constantly increases if \( y_i(t) > 0 \) at all times and the corresponding traffic light remains “red.”

Given the action \( \bar{\lambda}(t) \), the traffic dynamics given in (6) depend on the parameters \( p_i(\bar{\lambda}(t)) \) and \( q_{ij}(\bar{\lambda}(t)) \) associated with the action \( \bar{\lambda}(t) \), \( \Delta A(t) \in \mathbb{R}^{N \times N} \) covers possible uncertainties, \( U(t) \in \mathbb{Z}^{N_{a}}_{\geq 0} \) is the boundary inflow vector at time \( t \), and \( \Delta U(t) \in \mathbb{Z}^{N_{a}}_{\geq 0} \) models possible inflow uncertainties.

**Remark 4:** The boundary inflow \( U(t) \) is either uncontrollable or controlled. In the case of uncontrollable inlets, \( U(t) \) represents the nominal inflow learned from prior data, which, in general, is time-dependent, as it can be learned for different time intervals in a day (e.g., in the morning, in the evening, and so on). In this case, \( \Delta U(t) \) models possible imperfections. In the case of controlled inlet traffic flows, \( U(t) \) is the control input at time \( t \). Note that \( U(t) \) determines the available throughput in inlets, i.e., an upper bound on vehicles entering the network through each inlet. However, traffic demand might be less than the computed upper bounds, meaning that the utilized throughput is less than the available throughput. In this case, \( \Delta U(t) \) models differences between the available and utilized throughput.

Finally, due to the rounding function in (7), the impact of the uncertainty terms \( \Delta A(t) \) and \( \Delta U(t) \) can be expressed as an additive integer. More precisely, traffic dynamics given in (7) can be rewritten as
\[ x(t + 1) = \max \{[A(\bar{\lambda}(t))x(t) + BU(t)]_+ + d(t), 0\} \] (8)
where \( d(t) = [d_1(t) \cdots d_N(t)] \in D \forall t \) is the disturbance that is unknown but bounded, with \( D \subset \mathbb{Z}^N \) as a polyhedron containing the origin. Note that \( d_i(t) \) also models vehicles parking/unparking in lane \( i \).

**III. Emergency Vehicle-Centered Traffic Control—Centralized Scheme**

In this section, we will propose a centralized scheme whose algorithmic flowchart is given in Fig. 1. As seen in this figure, a central control unit determines the optimal inlet flows and configuration of all traffic lights. This implies that the data from all over the network should be available to the central unit at any \( t \).

In this section, we will use the following notations. Given the prediction horizon \([t, t + T_f]\) for some \( T_f \in \mathbb{Z}_{>0} \), we define
\[ U^t(t) = [U^t(t) \cdots U^t(t + T_f - 1)] \in \mathbb{Z}^{N_{a}}_{\geq 0} \], where \( U^t(t + k) \in \mathbb{Z}^{N_{a}}_{\geq 0} \) is the boundary inflow vector for time \( t + k \) (with \( k \leq T_f - 1 \)) computed at time \( t \). Also, \( \bar{\lambda'}^t(t + k) = \{\bar{\lambda}'(t), \ldots, \bar{\lambda}'(t + T_f - 1)\} \in \Lambda_{T_f} \), where \( \bar{\lambda}'(t + k) \) is the configuration of all traffic lights for time \( t + k \) (with \( k \leq T_f - 1 \)) computed at time \( t \). Note that \( * \) is added to the abovementioned notations to indicate optimal decisions.

**A. Normal Traffic Mode**

The normal traffic mode corresponds to traffic scenarios in which there is no emergency vehicle. Given the prediction horizon \([t, t + T_f]\), the control objective in a normal traffic
mode is to determine boundary inflows and configurations of traffic lights over the prediction horizon such that traffic congestion is alleviated in all lanes. This objective can be achieved through the following two-step receding horizon control, that is, the central unit computes the optimal boundary inflows and configuration of traffic lights over the prediction horizon by solving the associated optimization problems at every time instant \( t \), but only implements the next boundary inflows and configuration of traffic lights, and then solves the associated optimization problems again at the next time instant, repeatedly.

1) **Step 1:** Consider \( \hat{\lambda}_{t+T_f-2} \), \( \hat{\lambda}(t + T_f - 1) \), where \( \hat{\lambda}_{t+T_f-2} \) is the optimal solution\(^1\) of (11) obtained at time \( t - 1 \) and \( \hat{\lambda}(t + T_f - 1) \) is selected randomly from the action space \( \Lambda \). Then, the optimal boundary inflows over the prediction horizon \([t, t + T_f]\) (i.e., \( U_{t+T_f-1}^{t,*} \)) can be obtained by solving the following optimization problem:

\[
\begin{align*}
\min_{\theta} & \quad \sum_{k=0}^{T_f-1} \left( \| \hat{x}_{df}(k|t) \|_{\Gamma_x}^2 + \| U(t + k) - U_{\text{nom}}(t + k) \|_{\Theta}^2 \right) \\
\text{subject to} & \quad \hat{x}(k|t) \subseteq \tilde{\mathcal{X}}, \quad k = 1, \ldots, T_f \\
& \quad U(t + k) \in \mathbb{Z}_{\geq 0}^n, \quad k = 0, \ldots, T_f - 1 \quad (9\text{a})
\end{align*}
\]

where \( \mathcal{X} = \mathcal{X}^T \geq 0 \in \mathbb{R}^{n_a \times n_a} \) is a weighting matrix, \( \tilde{\mathcal{X}} \subset \mathbb{Z}_{\geq 0}^n \) is a polyhedron containing the origin,\(^2\) and

\[
\hat{x}(k + 1|t) \in \left( A(\hat{\lambda}^{t-1,*}(t + k)) \hat{x}(k|t) + B U(t + k) \right) \oplus D \\
(10)
\]

with initial condition \( \hat{x}(0|t) = x(t) \) and \( \hat{\lambda}^{t-1,*}(t + T_f - 1) = \hat{\lambda}(t + T_f - 1) \), which is selected randomly from the action space \( \Lambda \). Note that, to account for the disturbance \( d(t) \), (10) uses the Minkowski set sum of nominal predictions plus the set of all possible effects of the disturbance \( d(t) \) on the traffic density. The subscript "df" in (9a) stands for disturbance-free, and \( \hat{x}_{df}(k|t) \) can be computed via (10) by setting \( D = \{0\} \). The \( U_{\text{nom}}(t) \) is the nominal boundary inflow at time \( t \), which can be estimated based on prior traffic data. In (9), \( \Gamma_n = \text{diag} (\gamma_n, \ldots, \gamma_n) \), where \( \gamma_n \geq 0 \ \forall i \in \{1, \ldots, N\} \) is a design parameter that can be used to prioritize lanes. As suggested by the U.S. Department of Transportation [42], the prioritizing parameters can be determined according to total crashes and congestion over a specified period of time (e.g., over a five-year period); the higher the prioritizing parameter is, the higher priority is given to the density alleviation.

In summary, Step 1 computes the optimal boundary inflows by solving the optimization problem (9), which has \( T_f \times N_a \) integer decision variables constrained to be nonnegative and has \( T_f \times N \) inequality constraints on traffic density.

2) **Step 2:** Given \( U_{t+T_f-1}^{t,*} \) as the optimal solution of (9) obtained at time \( t \), the optimal configuration of all traffic lights over the prediction horizon \([t, t + T_f]\) (i.e., \( \hat{\lambda}_{t+T_f-1}^{t,*} \)) can be determined by solving the following optimization problem:

\[
\begin{align*}
\min_{\lambda} & \quad \sum_{k=0}^{T_f-1} \left( \| \hat{x}_{df}(k|t) \|_{\Gamma_x}^2 \right) \\
\text{subject to} & \quad \hat{x}(k|t) \subseteq \tilde{\mathcal{X}}, \quad k = 1, \ldots, T_f \\
& \quad \lambda(t + k) \in \Lambda, \quad k = 0, \ldots, T_f - 1 \quad (11\text{a})
\end{align*}
\]

where \( \tilde{\mathcal{X}} \subset \mathbb{Z}_{\geq 0}^n \) is a polyhedron containing the origin, and

\[
\hat{x}(k + 1|t) \in \left( A(\lambda(t + k))\hat{x}(k|t) + B U(t + k) \right) \oplus D \\
(12)
\]

with the initial condition \( \hat{x}(0|t) = x(t) \). Note that \( x_{df}(k|t) \) can be computed via (12) by setting \( D = \{0\} \). Note that, similar to (10), a set-valued prediction of traffic density by taking into account all possible realizations of the disturbance \( d(t) \) is considered in (12) to account for the disturbance \( d(t) \).

In summary, Step 2 determines the optimal configuration of traffic lights across the network by solving the optimization problem (11), which has \( T_f \) decision variables (each one is an \( M \)-tuple representing the configuration of traffic lights) constrained to belong to the set \( \Lambda \) (see Section II-B) and has \( T_f \times N \) inequality constraints on traffic density.

**Remark 5:** The cost function in (9) has two terms. The first term penalizes traffic density in all lanes of the network, and the second term penalizes the difference between the inlet traffic flows and their nominal values. It should be noted that a sufficiently large matrix \( \Theta \) guarantees that vehicles will never be blocked behind the network gates. A different method [19] to ensure that vehicles will not be blocked is to constrain the total boundary inflow to be equal to a certain amount, i.e., \( \sum_{i \in N_e} u_i(t) = \bar{u} \forall t \), where \( \bar{u} \) can be determined based upon prior traffic data. It is noteworthy that the computed optimal inflows can be implemented by means of network gates, i.e., ramp meters [37], [38] for highways and metering gates [39] for urban streets.

**Remark 6:** The prediction given in (10) provides an approximation to system (8), and the traffic density may take noninteger and/or negative values. However, as will be shown later, this approximation is efficient in ensuring optimality. The main advantage of using such an approximation is that the integer programming as in (9) can be easily solved by available tools.

**Remark 7:** The optimization problem (11) can be solved by using the brute-force search [43] (a.k.a. exhaustive search or generate & test) algorithm. Note that the size of the problem (11) is limited since \( \Lambda^{T_f} \) and \( D \) are finite. However, there are some techniques to reduce the search space and, consequently, speed up the algorithm. For instance, if the configuration \( \hat{\lambda}^{t+T_f-1}_{t+T_f-1} \) is infeasible and causes congestion at time \( t + k \) (with \( 0 \leq k \leq T_f - 1 \)), all configurations with the same first \( k - 1 \) actions will be excluded from the search space. Our simulation studies show that this simple step can largely reduce the CT of the optimization problem (11) (in our case, from 10 s to 8 ms).

**Remark 8:** In the case of uncontrolled boundary inflow, the proposed scheme for the normal traffic mode reduces to solving only the optimization problem (11) based upon learned nominal boundary inflows.
Remark 9: We assume that constraints on the traffic density are defined such that the resulting optimization problems are feasible. However, in the case of infeasibility, we can use standard methods (e.g., introducing slack variables) to relax constraints.

B. Emergency Traffic Mode

Suppose that the following holds.

1) At time $t = t_o$, a notification is received by the central control unit, indicating that an emergency vehicle will enter the network in $T_o$ time steps. Note that, for $t < t_o$, the condition of the network was normal.

2) Given the entering and leaving lanes, let $P$ represent the set of all possible paths for the emergency vehicle. Once the notification is received, i.e., at time $t = t_o$, based on the current and predicted traffic conditions, the optimal emergency path $I_o$ should be selected by the central control unit (see Remark 14) and be given to the emergency vehicle. We assume that the emergency vehicle will follow the provided path.

3) The emergency vehicle should leave the network in maximum $T_o$ time steps.

4) Once the emergency vehicle leaves the network, the traffic density in all lanes should be recovered to the normal traffic mode in $T_o$ time steps. This phase will be referred to as the recovery phase in the rest of this article.

Remark 10: $T_o$, $T_o'$, and $T_o''$ are specified at time $t$. These values can be computed by leveraging connectivity between the emergency vehicle and the roadside infrastructure. Note that these variables are time-variant, as they should be recomputed based on the traffic condition and position of the emergency vehicle at any $t$. For instance, once the emergency vehicle enters the network, $T_o$ should be set to zero, and once the emergency vehicle leaves the network, $T_o''$ should be set to zero. Also, when the recovery phase ends, $T_o''$ will be zero.

The control objective in an emergency traffic mode is to shorten the traveling time of the emergency vehicle, i.e., to help the emergency vehicle traverse the network as quickly and efficiently as possible. Given the emergency path with length $L$, the traveling time of the emergency vehicle can be estimated [44], [45] as

$$\text{Traveling Time} = \frac{L}{V_d} + \beta \times \text{Traffic Density on the Path}$$

for some constant $\beta > 0$, where $V_d$ is the desired traverse velocity. This relationship indicates that, for fixed $L$ and $V_d$, to shorten the traveling time of the emergency vehicle, one would need to reduce the traffic density on the emergency path.

Therefore, in an emergency traffic mode, given the prediction horizon $[t, t + T_f]$ with $T_f \geq T_o + T_o' + T_o''$, the control objective can be achieved by determining boundary inflows and configuration of all traffic lights such that: 1) during the time interval $[t, t + T_o + T_o']$, the traffic density in emergency path (DEP) should be reduced as much as possible, while the traffic density in other lanes is less than a certain amount; 2) during the time interval $[t + T_a' + T_o' + T_o'' + T_f']$, the traffic density in all lanes should be recovered to the normal traffic mode; and 3) during the time interval $[t + T_o' + T_o'' + T_f']$, the traffic density in all lanes should satisfy constraints of the normal mode.

We propose the following two-step receding horizon control approach to satisfy the abovementioned objectives. In this approach, the central unit computes the optimal boundary inflows and configuration of traffic lights over the prediction horizon by solving the associated optimization problems at every time instant $t$, but only implements the next boundary inflows and configuration of traffic lights, and then solves the associated optimization problems again at the next time instant, repeatedly.

1) Step 1: Consider $\{\lambda_{t+T_f-1}^{(t-1),*}, \lambda(t + T_f - 1)\}$, where $\lambda_{t+T_f-1}^{(t-1),*}$ is the optimal solution of (16a) obtained at time $t - 1$, and $\lambda(t + T_f - 1)$ is selected randomly from the action space $\Lambda$. Then, the optimal boundary inflows over the prediction horizon $[t, t + T_f]$ (i.e., $U_{t+T_f-1}^{(t),*}$) can be computed by solving the following optimization problem:

$$\min_{U} \sum_{k=0}^{T_o-1} \left( ||\tilde{z}_{df}(k)\|_{T_o}^2 + \|U(t + k) - U_{nom}(t + k)\|^2_{\max} \right)$$

subject to $\tilde{z}(t) \leq \tilde{z}_{t}^+$, $k = 1, \ldots, T_o + T_o' + T_o''$ (14a)

$\tilde{z}(t) \leq \tilde{z}_{t}^-$, $k = T_o' + T_o'' + T_f' + 1, \ldots, T_f$ (14b)

$U(t + k) \in \mathbb{Z}_{\geq 0}^N$, $k = 0, \ldots, T_f - 1$ (14c)

where $\tilde{z}(k)$ is the same as in (10), $\tilde{z}_{t}^+ \supset \tilde{z}_{t}^-$ is the extended constraint set (see Remark 12), $\Gamma_r = \text{diag}(|\gamma_{I}^{n}(k)|, \ldots, |\gamma_{N}^{n}(k)|)$ (see Remark 13) with

$$\gamma_{I}^{n}(k) = \begin{cases} \gamma_r, & \text{if } i \in I^*_n \text{ and } k \leq T_o' + T_o'' \\ \gamma_{I}^{n}, & \text{otherwise} \end{cases}$$

with $\gamma_r \gg \max_{i} |\gamma_{I}^{n}|$, and $I^*_n$ is the selected emergency path (see Remark 14). The prioritizing parameters, as in (15), ensure that the traffic density in the lanes included in the emergency path will be alleviated with a higher priority in the emergency traffic mode.

Similar to (9), the optimization problem (14) has $T_f \times N_{in}$ integer decision variables constrained to be nonnegative and has $T_f \times N$ inequality constraints on the traffic density.

2) Step 2: Given $U_{t+T_f-1}^{(t),*}$ as the optimal solution of (14) obtained at time $t$, the optimal configurations of the traffic lights over the prediction horizon $[t, t + T_f]$ (i.e., $\lambda_{t+T_f-1}^{(t),*}$) can be obtained as the optimal solution of (11) at time $t$.

Since the traffic condition was normal for $t < t_o$, $\lambda_{t+T_f-1}^{(t-1),*}$ is the optimal solution of (11) at time $t$. 

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be determined by solving the following optimization problem:

$$\min_{\lambda} \sum_{k=0}^{T_f-1} \| \tilde{x}_{df}(k|t) \|_1^2, \quad (16a)$$

subject to

$$\tilde{x}(k|t) \subseteq \tilde{X}^+, \quad k = 1, \ldots, T'_{d} + T'_{s} + T'_{r}$$

$$\tilde{x}(k|t) \subseteq \tilde{X}, \quad k = T'_{d} + T'_{s} + T'_{r} + 1, \ldots, T_f$$

$$\lambda(t + k) \in \Lambda, \quad k = 0, \ldots, T_f - 1$$

where $\tilde{x}(k|t)$ is as in (12), and $\tilde{X}^+ \supset \tilde{X}$ is the extended set (see Remark 12). Similar to (11), the optimization problem (16a) has $T_f$ decision variables (each one is an $M$-tuple representing the configuration of traffic lights) constrained to belong to the set $\Lambda$ (see Section II-B) and has $T_f \times N$ inequality constraints on the traffic density.

**Remark 11:** The optimization problem (14) can be solved by mixed-integer tools, and the optimization problem (16a) can be solved by using the brute-force search algorithms.

**Remark 12:** We assume that constraints on the traffic density can be temporarily relaxed. This assumption is reasonable [46], [47], as, in practice, constraints are often imposed conservatively to avoid congestion. In mathematical terms, by relaxation, we mean that the traffic density should belong to extended sets $\tilde{X}^+ \supset \tilde{X}$ and $\tilde{X} \supset \tilde{X}$. This relaxation enables the control scheme to put more effort into the alleviation of traffic DEP. This relaxation can last up to maximum $T'_{d} + T'_{s} + T'_{r}$ time steps.

**Remark 13:** $\Gamma$ as in (15) prioritizes alleviating traffic density in lanes included in the emergency path $I'_e$ during the time interval in which the emergency vehicle is traversing the network, i.e., the time interval $[t, t + T'_{d} + T'_{s}]$.

**Remark 14:** Once the emergency notification is received by the central control unit (i.e., at time $t = t_e$), the optimization problems (14) and (16a) should be solved for all possible paths, i.e., for each element of $\mathcal{P}$. Then: 1) according to (13), the optimal emergency path $I'_e$ should be selected as

$$I'_e = \arg \min_{I_e \in \mathcal{P}} \sum_{k=1}^{T'_{d} + T'_{s}} \sum_{i \in I_e} x_{i,df}(k|t_e)$$

and 2) the boundary inflow and configuration of traffic lights at time $t = t_e$ will be the ones associated with the optimal emergency path $I'_e$.

**Remark 15:** Once the recovery phase ends, the traffic condition will be normal, and the boundary inflow vector and configuration of traffic lights should be determined through the two-step control scheme presented in Section III-A.

**Remark 16:** In the case of uncontrolled boundary inflow, the proposed scheme for the emergency traffic mode reduces to solving only the optimization problem (16a) based upon learned nominal boundary inflows.

### IV. EMERGENCY VEHICLE-CENTERED TRAFFIC CONTROL—DECENTRALIZED SCHEME

In this section, we will develop a decentralized traffic control scheme whose algorithmic flowchart is depicted in Fig. 2. In the decentralized scheme, there is a control unit at each intersection, which controls the configuration of the traffic lights at that intersection, as well as the traffic flow in the corresponding inlets. During each sampling period, an aggregator receives data from all control units, augments data, and shares it across the network. This is reasonable for real-time applications even with cheap and relatively high-latency communication technologies, as the duration of the traffic light states is large (e.g., 30 s). In Section V, we will characterize the optimality of the developed decentralized scheme in our numerical experiments in different traffic modes in comparison with the centralized scheme.

The main advantage of the decentralized scheme is that the size of the resulting optimization problem is very small compared to that of the centralized scheme, as it only needs to determine the configuration of traffic lights and inlet traffic flows at one intersection. This greatly reduces the CT for large networks even though it may slightly degrade performance. This will be discussed in Section V.

In this section, we use $\lambda(t) \in \mathbb{R}^N$, $j \in \mathcal{M}$ (with $N_j \leq N$) to denote traffic density in lanes controlled by Control Unit$j$. Also, $\lambda(t) \in \mathbb{R}^N$, $j \in \mathcal{M}$ is the traffic inflow vector at time $t$ in the network, $\lambda(t) \in \mathbb{R}^N$, $j \in \mathcal{M}$ is the traffic density in lanes associated with intersection $I_j$ for time $t$ (with $k \leq T_f - 1$) computed at time $t$, and $i(j(t+1), \ldots, j'(t+1)) = \lambda(t), \ldots, \lambda(t+1)$ is the configuration of traffic lights at intersection $I_j$ for time $t+1$ (with $k \leq T_f - 1$) computed at time $t$. Note that $\sum_j N^m_j = N^m$, and $\mathcal{S}$ in the superscript of the abovementioned notations indicates optimal decisions.

#### A. Normal Traffic Mode

As discussed in Section III-A, the control objective in a normal traffic mode is to alleviate traffic density across the network. During the time interval $[t-1, t)$, all control units receive $i(j(t-1), \ldots, j'(t-1))$ and $\lambda_{t-1}^j$, $j'_{t-1}^j$, $\lambda_{t-1}^j$ for all $j \in \mathcal{M}$, $x(t-1)$, $U_{x,t-1}^j$, $\ldots$, $\lambda_{t-1}^j$ (with $k \leq T_f - 1$) computed at time $t$, and $\lambda_{t-1}^j, \ldots, \lambda_{t-1}^j$ is the configuration of traffic lights at intersection $I_j$ for time $t+1$ (with $k \leq T_f - 1$) computed at time $t$. Note that $\sum_j N^m_j = N^m$, and $\mathcal{S}$ in the superscript of the abovementioned notations indicates optimal decisions.

1. Compute $x(t|t-1)$ based on the shared information by the aggregator and according to (8) with $d(t-1) = 0$.
2. Update traffic density at local lanes [i.e., $\lambda(t)$], and replace corresponding elements in $x(t|t-1)$ with updated values.
3. Compute $i(j(t-1), \ldots, j'(t-1))$ for all $j \in \mathcal{M}$, where $i(j(t-1), \ldots, j'(t-1))$ is the optimal solution of Control Unit$j$ obtained at time $t-1$, and $\lambda(t+T_f-1)$ is selected randomly from the action space $\Lambda$.
4. Compute $i(U_{x,t-1}^j, \ldots, U_{x,T_f-1}^j)$ for all $i \in \mathcal{M}$ and $i \neq j$, where $i(U_{x,t-1}^j, \ldots, U_{x,T_f-1}^j)$ is the optimal solution of Control Unit$i$ obtained at time $t-1$.  

$\lambda_{t-1}^j, \lambda_{t-1}^j$ should be selected randomly from the action space $\Lambda^j_{T_f-1}$.

$\lambda_{t-1}^j, \lambda_{t-1}^j$ is $\lambda_{t-1}^j(t+T_f-2)$.
5) Solve the following optimization problem to determine the inlet traffic flows at intersection \( I_j \) over the prediction horizon \( [t, t + T_f] \) (i.e., \( j U_{t_t+1}^t \)):

\[
\min_{jU} \sum_{k=0}^{T_f-1} \left( \| j \dot{x}(k|t) \|^2_{\Gamma_{t_k}} + \| j U(t + k) - j U_{nom}(t + k) \|^2_{\Theta} \right) \tag{18a}
\]

subject to \( j \dot{x}(k|t) \subseteq j \bar{X}, \quad k = 1, \ldots, T_f \) \tag{18b}

where \( j \Gamma_n = j \Gamma_n^T \geq 0 \) (in \( \mathbb{R}^{N_j} \)) and \( j \Theta = j \Theta^T \geq 0 \) (in \( \mathbb{R}^{N_j \times N_j} \)) are weighting matrices, \( j \dot{x}(k|t) \) can be computed via (10) with initial condition \( x(t|t-1) \), and \( j \bar{X} \subseteq \mathbb{R}^{N_j} \) is a polyhedron containing the origin. The optimization problem (18) has \( T_f \times N_j \) integer decision variables constrained to be nonnegative and has \( T_f \times N_j \) inequality constraints on the traffic density.

6) Given \( j U_{t_t+1}^t \) as the optimal solution of (18) obtained at time \( t \), solve the following optimization problem to determine the configuration of traffic lights at intersection \( I_j \) over the prediction horizon \( [t, t + T_f] \) (i.e., \( j \lambda_{t_t+1}^t \)):

\[
\min_{j \lambda} \sum_{k=0}^{T_f-1} \left( \| j \dot{X}(k|t) \|^2_{\Gamma_{\lambda_k}} \right) \tag{19a}
\]

subject to \( j \dot{X}(k|t) \subseteq j \bar{X}, \quad k = 1, \ldots, T_f \) \tag{19b}

where \( j \dot{X}(k|t) \) can be computed via (12) with initial condition \( x(t|t-1) \), and \( j \bar{X} \subseteq \mathbb{R}^{N_j} \) is a polyhedron containing the origin. The optimization problem (19) has \( T_f \times \Lambda_j \) decision variables constrained to belong to the set \( \Lambda_j \) (see Section II-B) and has \( T_f \times N_j \) inequality constraints on the traffic density.

Note that the abovementioned scheme is receding horizon control-based, that is, the Control Unit\#\( j, j \in \mathcal{M} \) computes the optimal inlet traffic flows and configuration of the traffic lights at intersection \( I_j \) over the prediction horizon by solving the associated optimization problems at every time instant \( t \), but only implements the next inlet traffic flows and configuration of traffic lights, and then solves the associated optimization problems again at the next time instant, repeatedly.

Remark 17: The optimization problem (18) can be solved by mixed-integer tools, and the optimization problem (19) can be solved by using the brute-force search algorithms.

Remark 18: In the decentralized scheme, Control Unit\#\( j, j \in \mathcal{M} \) estimates the traffic density at time \( t \) across the network by assuming \( d(t-1) = 0 \). Thus, in general, \( x(t|t-1) \neq x(t) \). Also, Control Unit\#\( j \) determines the optimal decisions over the prediction horizon based upon the optimal decisions of other control units at time \( t - 1 \). As a result, the decentralized scheme is expected to provide a suboptimal solution. This will be shown in Section V.

B. Emergency Traffic Mode

Consider the assumptions mentioned in Section III-B regarding the arriving, leaving, and recovery times. The control objective in an emergency traffic mode is to shorten the travel time of the emergency vehicle without causing congestion in other lanes. Given \( T_f^0, T_f^1, \) and \( T_f^2 \) by the aggregator, the Control Unit\#\( j, j \in \mathcal{M} \) executes the following steps to determine the inlet traffic flows and configuration of the traffic lights at intersection \( I_j \) in an emergency traffic mode:

1) Compute \( x(t|t-1) \) based on the shared information by the aggregator and according to (8) with \( d(t-1) = 0 \).
2) Update traffic density at local lanes (i.e., \( \dot{x}(t) \)), and replace corresponding elements in \( x(t|t-1) \) with updated values.
3) Compute \( j \lambda_{t_t+1}^t, \lambda_i(t+T_f-1) \) for all \( i \in \mathcal{M} \), where \( j \lambda_{t_t+1}^t \) is the optimal solution of Control Unit\#\( i \) obtained at time \( t - 1 \) and \( \lambda_i(t+T_f-1) \) is selected randomly from the action space \( \Lambda_i \).
4) Compute \( j \dot{X}(t|t-1) \) for all \( i \in \mathcal{M} \) and \( i \neq j \), where \( j \dot{X}(t|t-1) \) is the optimal solution of Control Unit\#\( i \) obtained at time \( t - 1 \).
5) Solve the following optimization problem to determine the inlet traffic flows at intersection \( I_j \) over the prediction horizon \([t, t + T_f]\) (i.e., \( jU_{t, t+T_{n-1}} \)):

\[
\min_{jU} \sum_{k=0}^{T_f-1} \left( \|j\tilde{x}_{df}(k|t)\|^2_{T_{f,k}} + \|jU(t + k) - jU_{nom}(t + k)\|^2_{T_{f,k}} \right) \tag{20a}
\]

subject to

\[
\begin{align*}
&j\tilde{x}(k|t) \subseteq j\tilde{x}^+ \\
&k = 1, \ldots, T_j^d + T_j^s + T_f \\
&j\tilde{x}(k|t) \subseteq j\tilde{x} \\
&k = T_j^d + T_j^s + T_f^i + 1, \ldots, T_f \\
&jU(t + k) \in \mathbb{Z}_{\geq 0}^N_j, \quad k = 0, \ldots, T_f - 1
\end{align*} \tag{20b}
\]

where \( j\tilde{x}^+ \subseteq j\tilde{x} \) is the extended set (see Remark 12), and \( T_{f,k} = jU_{t, t+T_{n-1}} \geq 0 \) (\( \in \mathbb{R}^N_j \)) is the weighting matrix (see Remark 13). Similar to (18), the optimization problem (20) has \( T_f \times N_j \) integer decision variables constrained to be nonnegative and has \( T_f \times N_j \) inequality constraints on traffic density.

6) Given \( jU_{t, t+T_{n-1}} \) as the optimal solution of (20) obtained at time \( t \), solve the following optimization problem to determine the configuration of traffic lights at intersection \( I_j \) over the prediction horizon \([t, t + T_f]\) (i.e., \( jU_{t, t+T_{n-1}} \)):

\[
\min_{\lambda_j} \sum_{k=0}^{T_f-1} \|j\tilde{x}_{df}(k|t)\|^2_{T_f,k} \tag{21a}
\]

subject to

\[
\begin{align*}
&j\tilde{x}(k|t) \subseteq j\tilde{x}^+ \\
&k = 1, \ldots, T_j^d + T_j^s + T_f \\
&j\tilde{x}(k|t) \subseteq j\tilde{x} \\
&k = T_j^d + T_j^s + T_f^i + 1, \ldots, T_f \\
&\lambda_j(t + k) \in \Lambda_j, \quad k = 0, \ldots, T_f - 1
\end{align*} \tag{21b}
\]

where \( j\tilde{x}^+ \subseteq j\tilde{x} \) is the extended set (see Remark 12). Similar to (19), the optimization problem (21) has \( T_f \) decision variables constrained to belong to the set \( \Lambda_j \) (see Section II-B) and has \( T_f \times N_j \) inequality constraints on the traffic density.

Remark 19: The optimization problem (20) can be solved by mixed-integer tools, and the optimization problem (21) can be solved by using the brute-force search algorithms.

Remark 20: In the decentralized scheme, the emergency path \( I_{se} \) is determined by the emergency vehicle and is shared with control units through the aggregator.

Remark 21: In this article, we assume that each control unit in the decentralized scheme controls the inlet traffic flows and configuration of traffic lights at one intersection. However, the decentralized scheme is applicable to the case where a network is divided into some subnetworks, and there exists a control unit in each subnetwork controlling the entire subnetwork.

V. SIMULATION RESULTS

Consider the traffic network shown in Fig. 3. This network contains 14 unidirectional lanes identified by the set \( \mathcal{N} = \{1, \ldots, 14\} \) and four intersections identified by the set \( \mathcal{M} = \{1, \ldots, 4\} \). Also, \( \mathcal{N}_{in} = \{2, 7, 8\} \) and \( \mathcal{N}_{out} = \{1, 3, 4\} \). The possible configurations of traffic lights at each intersection of the traffic network shown in Fig. 3 are as follows: 1) intersection \( I_1 \): \( \lambda_{1,1} \) corresponds to a “green” light at the end of lane 8 and a “red” light at the end of lane 12; \( \lambda_{1,2} \) corresponds to a “red” light at the end of lane 8 and a “green” light at the end of lane 12; 2) intersection \( I_2 \): \( \lambda_{2,1} \) corresponds to a “green” light at the end of lane 10 and a “red” light at the end of lane 2; \( \lambda_{2,2} \) corresponds to a “red” light at the end of lane 10 and a “green” light at the end of lane 2; 3) intersection \( I_3 \): \( \lambda_{3,1} \) corresponds to a “green” light at the end of lane 7 and a “red” light at the end of lane 13; \( \lambda_{3,2} \) corresponds to a “red” light at the end of lane 7 and a “green” light at the end of lane 13; 4) intersection \( I_4 \): \( \lambda_{4,1} \) corresponds to a “green” light at the end of lane 14 and a “red” light at the end of lane 11; \( \lambda_{4,2} \) corresponds to a “red” light at the end of lane 14 and a “green” light at the end of lane 11.

The boundary inflow vector of the traffic network shown in Fig. 3 is \( U(t) = (u_2(t) \ u_5(t) \ u_8(t))^T \in \mathbb{R}^{3}_{\geq 0} \). We assume that \( \Delta T = 30 \text{ s} \); this sampling period is appropriate to address macroscopic characteristics of traffic flow [19], [48], [49], as the traffic cycle range from 1 to 3 min in real-world systems [31]. For intersection \( I_1 \) and the action \( \lambda = (\lambda_{1,1}, \lambda_{2,1}, \lambda_{3,1}, \lambda_{4,1}) \), we have \( p_{10}(\lambda) = 0 \), \( q_{8,1}(\lambda), q_{8,10}(\lambda), q_{8,13}(\lambda) \in [0, 1] \), and \( q_{12,11}(\lambda) = q_{12,10}(\lambda) = 0 \). For intersection \( I_1 \) and the action \( \lambda = (\lambda_{1,2}, \lambda_{2,2}, \lambda_{3,2}, \lambda_{4,2}) \), we have \( p_{10}(\lambda) = 0 \), \( q_{8,1}(\lambda), q_{8,10}(\lambda), q_{8,13}(\lambda) = 0 \), and \( q_{12,11}(\lambda) = q_{12,9}(\lambda) = q_{12,10}(\lambda) \in [0, 1] \). For intersection \( I_2 \) and the action \( \lambda = (\lambda_{1,1}, \lambda_{2,1}, \lambda_{3,1}, \lambda_{4,1}) \), we have \( p_{10}(\lambda) = 0 \), \( q_{8,1}(\lambda), q_{8,10}(\lambda), q_{8,13}(\lambda) \in [0, 1] \), and \( q_{2,3}(\lambda) = q_{2,11}(\lambda) = 0 \). For intersection \( I_2 \) and the action \( \lambda = (\lambda_{1,2}, \lambda_{2,2}, \lambda_{3,2}, \lambda_{4,2}) \), we have \( p_{10}(\lambda) = 0 \), \( q_{8,1}(\lambda), q_{8,10}(\lambda) \in [0, 1] \), and \( q_{2,3}(\lambda) = q_{2,11}(\lambda) = 0 \).
considered traffic network. The action space is $\Lambda = \{\lambda_1, \lambda_2, \lambda_3, \lambda_4\}$, where $\Lambda_1 = \{\lambda_1, \lambda_1\}$, $\Lambda_2 = \{\lambda_2, \lambda_2\}$, $\Lambda_3 = \{\lambda_3, \lambda_3\}$, and $\Lambda_4 = \{\lambda_4, \lambda_4\}$.

$\lambda = (\lambda_1, \lambda_2, \lambda_3, \lambda_4)$, we have $p_{13}(\lambda) = 0$, $p_{17}(\lambda) \in [0, 1]$, $q_{13}(\lambda), q_{13, 14}(\lambda) = 0$, and $q_{12, 14}(\lambda) = \gamma_{q12}(\lambda) = \gamma_{q13}(\lambda) \in [0, 1]$. For intersection $I_3$ and the action $\lambda = (\lambda_1, \lambda_2, \lambda_3, \lambda_4)$, we have $p_{13}(\lambda) = 0$, $p_{13}(\lambda) \in [0, 1]$, $q_{13}(\lambda), q_{13, 14}(\lambda) = 0$, and $q_{12, 14}(\lambda) = \gamma_{q12}(\lambda) = \gamma_{q13}(\lambda) = 0$. For intersection $I_4$ and the action $\lambda = (\lambda_1, \lambda_2, \lambda_3, \lambda_4)$, we have $p_{14}(\lambda) = 0$, $p_{11}(\lambda) = 0$, $q_{14, 14}(\lambda), q_{14, 15}(\lambda) = 0$, and $q_{11, 14}(\lambda) = q_{11, 15}(\lambda) = 0$.

For implementing the decentralized scheme, we assume that $x(t) = [x_1(t) x_8(t) x_9(t) x_{12}(t)]^T \in \mathbb{Z}_{\geq 0}^4$, $\tilde{x}(t) = [x_5(t) x_3(t) x_{10}(t)]^T \in \mathbb{Z}_{\geq 0}^3$, $\tilde{y}(t) = [x_6(t) x_7(t) x_{13}(t)]^T \in \mathbb{Z}_{\geq 0}^3$, and $\bar{x}(t) = [x_4(t) x_5(t) x_{14}(t)]^T \in \mathbb{Z}_{\geq 0}^4$. That is, Control Unit#1 controls lanes 1, 8, 9, and 12; Control Unit#2 controls lanes 2, 3, 10; Control Unit#3 controls lanes 6, 7, and 13; and Control Unit#4 controls lanes 4, 5, 11, and 14. Also, $U(t) = u_{S}(t)$, $\bar{U}(t) = u_{T}(t)$, and $\bar{U}(t) = u_{T}$. Thus, $N_{m}^{1} = 1, N_{N}^{0} = 1, N_{m}^{3} = 1$, and $N_{m}^{4} = 0$.

The simulations are run on an Intel® Core™ i7-7500U CPU 2.70 GHz with 16.00 GB of RAM. In order to have a visual demonstration of the considered traffic network, a simulator is generated (see Fig. 5). A video of the operation of the simulator is available at the URL: https://youtu.be/FmEYCxmD-Oc. For comparison purposes, we also simulate the centralized scheme presented in [19] and a typical/existing/usual/baseline traffic system (i.e., the system with the periodic schedule for traffic lights). Table II compares the mean CT of the proposed schemes per time step with that of the scheme presented in [19], where the value for the scheme of [19] is used as the basis for normalization. As can be seen from this table, the CT of the proposed centralized scheme is $\sim 1.5$ times less than that of the scheme of [19]. The CT of the proposed decentralized scheme is $\sim 1000$ times less than that of the scheme of [19] and is $\sim 800$ times less than that of the proposed centralized scheme.

A. Normal Traffic Mode

Let $\mathcal{X} = \{x|x_i \leq 20, i \in \{1, \ldots, 14\}\}$ and $d_i(t) \forall i$ be selected uniformly from $[-2, -1, 0, 1, 2]$. The initial condition is $x(0) = [15, 16, 15, 12, 12, 17, 18, 10, 10, 14, 12, 10, 16, 10]^T$, and the nominal boundary inflow is $U_{nom}(t) = [6, 6, 8]^T$. Also, $\Theta = 50N_{N}$, and $\gamma = 1 \forall i$.

Simulation results are shown in Fig. 6. Table III compares the achieved steady-state density (SSD) with the considered schemes, where the value for the typical/existing/usual/baseline traffic system is used as the basis for normalization. Note that the reports are based on results of 1000 runs. According to Table III, all methods perform better than the typical/existing/usual/baseline traffic system. The proposed centralized scheme provides the best response. The proposed decentralized scheme outperforms the scheme of [19], while, as expected, it yields a larger SSD compared to the proposed centralized scheme. More precisely, degradation in the mean SSD by the decentralized scheme in comparison with the centralized scheme in a normal traffic mode is

\begin{table}[h]
\centering
\caption{Comparing the Mean CT of the Proposed Schemes with That of Scheme of [40]}
\begin{tabular}{|c|c|c|}
\hline
Mean CT (Norm.) & Centralized & Decentralized & Scheme of [19] \\
\hline
0.734 & 1.03 $\times 10^{-3}$ & 1 \\
\hline
\end{tabular}
\end{table}
11.42%, which is small and acceptable in real-life traffic scenarios. Thus, the cost of using the decentralized scheme instead of the centralized scheme in a normal traffic mode is very small.

**B. Emergency Traffic Mode**

Suppose that, at time $t = 10$, the aggregator receives a notification that an emergency vehicle will enter the network through lane 8 in two time steps and should leave the network in two time steps through lane 5. Also, suppose that we have one time step to recover the traffic condition. We have $P = \{I_1^e, I_2^e\}$, where $I_1^e = \{8, 13, 14, 5\}$ and $I_2^e = \{8, 10, 11, 5\}$. Let $\hat{x}^+ = \tilde{x}^+ = \{x_i \leq 25\}$.

Simulation results are shown in Fig. 7, and the results from comparison analysis are reported in Table IV, which are computed based on results of 1000 runs. Note that the values for the typical/existing/usual/baseline traffic system are used as nominal values for normalization. As seen in Table IV, both schemes proposed in this article perform better than the typical/existing/usual/baseline traffic system in an emergency traffic mode. In particular, the centralized and decentralized schemes reduce the mean SSD by 23.73% and 14.58%, respectively. As expected, the decentralized scheme yields a larger SSD compared to the centralized scheme. More precisely, degradation in mean SSD by the decentralized scheme in comparison with the centralized scheme is 11.98%. Table IV also reports that the centralized and decentralized schemes reduce the mean DEP by 47.97% and 30.42%, respectively. It is noteworthy that the degradation in the mean DEP by the decentralized scheme in comparison with the centralized scheme is 33.73%.

**C. Sensitivity Analysis—Impact of Look-Ahead Horizon $T_f$**

Fig. 8 shows how the prediction window size impacts the performance and CT of the developed centralized scheme, where the values for $T_f = 1$ are used as bases for normalization. As $T_f$ increases, the performance improves at the cost of increased CT. For large $T_f$ the performance degrades due to poor prediction accuracy.
reduces. Fig. 8 (right) shows that, as the look-ahead horizon increases, the CT of the proposed decentralized scheme increases concomitantly with the size and complexity of the associated optimization problems. In the simulation studies, we selected $T_f = 4$, as it yields the best performance with an affordable computing time. Note that a similar behavior is observed for the centralized scheme, that is, $T_f = 4$ provides the best performance for the centralized scheme.

VI. CONCLUSION

This article proposed an emergency vehicle-centered traffic control framework to alleviate traffic congestion in a network of interconnected signaled lanes. The aim of this article is to integrate CMT with MPC to ensure that emergency vehicles traverse multiple intersections efficiently and timely. Two schemes were developed in this article: 1) centralized and 2) decentralized. It was shown that the centralized scheme provides the optimal solution even though its CT may be large for large networks. To cope with this problem, a decentralized scheme was developed, where an aggregator acts as the hub of the network. It was shown that the CT of the decentralized scheme is very small, which makes it a good candidate for large networks, even though it provides a suboptimal solution. Extensive simulation studies were carried out to validate and evaluate the performance of the proposed schemes.

Future work will aim at extending the developed schemes to deal with cases where two (or more) emergency vehicles traverse a network. This extension is not trivial and requires addressing many technical and methodological challenges. Also, future work should investigate the robustness and tolerance of the decentralized scheme to uncertainty in communication delay and communication failures.

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