Stability and performance evaluation of the speed control of DC motor using state-feedback controller

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ABSTRACT

Direct current (DC) motor are widely used in many applications due to its accurate control of speed and position. However, a proper control and operation is still required and might be a challenge for control designers. This paper presents the design of a state-feedback control to evaluate the performance of the speed control of DC motor for different applications. The simulation results were carried out with and without disturbance applied to the system. The proposed control method showed a stable system response with both cases of disturbances. Therefore, it can be used to solidate the control of DC motor in the real application.

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1. INTRODUCTION

Direct current (DC) motor a device which was designed to convert electrical power to mechanical power. Excited DC motor is one type of DC motors which was widely used to illustrate the dynamic performance of a typical DC motor behaviour. The DC motor can be controlled by common two methods: i) by changing the applied voltage to the armature or ii) changing the applied voltage to the field winding [1]-[3]. Industrial DC motors were applied to many applications like electric vehicles, cranes, steel rolling mills and robotic due to many advantages such as, simple, precise, and characteristics of continuous control [4]-[7].

The development of the motor drives is very demandable in different industrial applications such as steel rolling mills, electric trains and robotics [8], [9]. In addition, these drive systems must have an acceptable tracking for the dynamic speed command and load control response to perform different tasks. DC motor drives, thanks to their simplicity, easist application, high standard of reliabilities, more flexibilities and reasonable cost have long been integrated and involved in many industrial applications such as robot manipulators and domestic appliances with the target of speed and position control. DC motors are superior in control of speed for deceleration and acceleration. DC motors are preferable for most horsepower ratings due to their reasonable cost. Moreover, DC motors have had been widely uses as speed machines due to its adjustable mechanism. In such applications, the motor should be controlled using a good control algorithm to provide the desired response performance [10]-[13].
The design and implementation of the state feedback controller using Matlab/simulink for position control of DC motor was presented in [14]. This system was designed using dSPACE DS1104 board as well as real DC motor. The experimental results in testing the Maxon DC motor showed the effectiveness of the control scheme and the motor position can be controlled over certain range.

In addition, the design of robust state feedback controller was approached in time domain for the uncertain DC-motor system was proposed by [15]. The goal was to observe their state vectors because the output vector of this real system was measurable. The controlled plant model was the ‘polytopic’ model of uncertain system. The linear matrix inequality (LMI) region was used to measure the stability performance of the closed loop system, where the poles of whole uncertainty domain are placed. The Lyapunov function was used to improve the the quadratic stability [15]. Design and implementation of various robust controllers for DC motor speed control with fixed field and different position values and constant speed was proposed in [16]. The method provides minimum rise time, overshoot, and fast settling time versus low steady state error. The closed-loop feedback control with different load characteristics were validated using both MATLAB and experimental representation.

In control theory, state variable analysis covers the initial conditions and time-variant/invariant, linear/non-linear. Furthermore, single or multiple input output systems can also be analysed [17], [18]. The principle of feedback of all state variables feeding the input of the system was through a feedback matrix in the control strategy is preferable using full-state variable feedback control [19], [20]. State feedback is very useful for multi-input multi-output systems and for control systems with optimum constraints, such as those requiring a minimum time to final value or minimal control effort. The advantage of the state feedback method is that the controller parameters have a greater degree of freedom with respect to the output feedback method [21]-[24].

As explained above, DC motor has been used in too many applications due to simplicity of its mechanical structure to provide a superior response by controlling the position and speed. However, a proper control and operation is still an issue [14]. Therefore, the state feedback method was presented in this paper.

2. MODEL OF DC MOTOR

DC motors provide the capability of high torque. However, this function is generally referring to the actual physical size of the motor. In addition, are easy to be minimized and can be “throttled” by adjusting their supplied voltage. These motors are the simplest and oldest electrical motors and most commonly used machines for electromechanical energy conversion. The major advantages of these kinds’ motors are easy speed and torque regulation, Figure 1 shows the general layout of the DC motor model.

![Figure 1. General layout of Model of DC motor](image)

2.1. Equation of the system

The torque (\(T\)) is referring to the armature current (\(i_a\)) by using constant of the torque (\(K_T\)),

\[
T = K_T i_a
\]  

(1)

the generated voltage is referred by (\(V_{emf}\)) and also is relating to the angular velocity (\(\omega\)) by,

\[
V_{emf} = K_w \omega = K_w \frac{d\theta}{dt}
\]  

(2)

by using Figure 1, and based on the Newton’s law as well as the Kirchhoff’s law the following equations can be written,

\[
J \frac{d^2\theta}{dt^2} + B \frac{d\theta}{dt} = K_T i_a
\]  

(3)

\[
L \frac{di_a}{dt} + R i_a = V_a - K_w \frac{d\theta}{dt}
\]  

(4)

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using the Laplace transform, as shown in (3) and (4) can be written as,

\[ Js^2 \theta(s) + Bs \theta(s) = K_T I_a(s) \quad (5) \]

\[ L s I_a(s) + R I_a(s) = V_a(s) - K_{oa} s \theta(s) \quad (6) \]

from shown in (6) we can express \( I_a(s) \),

\[ I_a(s) = \frac{V_a(s) - K_{oa} s \theta(s)}{R + L s} \quad (7) \]

and substitute as shown in (7) in (5), we get,

\[ Js^2 \theta(s) + Bs \theta(s) = K_T \frac{V_a(s) - K_{oa} s \theta(s)}{R + L s} \quad (8) \]

From shown in (8), the transfer function for angular velocity with respect to the input voltage \( G_m(s) \) can be got,

\[ G_m(s) = \frac{\hat{\theta}(s)}{V_a(s)} = \frac{K_T}{(R + L s)(Js + B) + K_T K_{oa}} \quad (9) \]

DC motor parameters are presented using Table 1 [25],

| Parameter | Value |
|-----------|-------|
| \( R \)   | 4.67  |
| \( L \)   | 0.17 H |
| \( J \)   | 0.0426 e-3 Kgm² |
| \( B \)   | 0.0473 e-3 Nm·rad/ sec |
| \( K_T \) | 0.0147 Nm/A |
| \( K_{oa} \) | 0.0147 V/sec·rad |

The ‘transfer function’ \( G_m \) for (DC) Motor, which represented the angular velocity with respect to input voltage is,

\[ G_m(s) = \frac{2030}{s^2 + 28.58 s + 60.34} \]

3. STATE_FEEDBACK_CONTROLLER DESIGN

By Considering the state-space model of a (SISO system) shown in Figure 2 and (10).

\[ x(k + 1) = A x(k) + B u(k) \]
\[ y(k) = C x(k) \quad (10) \]

where \( x(k) \in \mathbb{R}^n \), \( u(k) \) and \( y(k) \) are scalar. The states are located in feedback to the input location in order to have desired locations for the closed poles.

Affine State Feedback Law is,

\[ u(k) = -K x(k) + v(k) \quad (11) \]

where \( v(k) \) is the reference input and \( K \) (state feedback gain) is \( \mathbb{R}^{1 \times n} \)

If \( v(k) \neq 0 \), the goal of the control design is the tracking, if \( v(k) = 0 \), the design problem is known as regulation problem and state feedback law (control input) became,

\[ u(k) = -K x(k) \quad (12) \]

the state feedback control was also designed using pole placement control as shown in Figure 3. Substitute as shown in (12) in (10);

\[ x(k + 1) = (A - BK) x(k) \quad (13) \]
The problem of the regulation will be solved if \( K \) is designed with eigenvalues of \( A - BK \) are located within the unit circle of the system. The closed loop poles of the system shown in (13) are place in desired locations by the control law, for this reason the state feedback gain matrix \( K \) is design. Therefore, the pair \((A, B)\) must be controllable for accurate condition of arbitrary pole placement and all states are located in feedback to the input side (assume measurable). Transforming the state model into canonical form is shown in (14). The controllability matrix is written as \( M_C \) and the transformation matrix is \( T \):

\[
T = MC_H
\]

where,

\[
H = \begin{bmatrix}
a_{n-1} & a_{n-2} & \cdots & a_1 & 1 \\
a_{n-2} & a_{n-3} & \cdots & 1 & 0 \\
\vdots & \vdots & \ddots & \vdots & \vdots \\
a_1 & 1 & \cdots & 0 & 0 \\
1 & 0 & \cdots & 0 & 0
\end{bmatrix}
\]

\(a_i\) are the characteristic coefficients \( [\zeta] I - A = z^n + a_1 z^{n-1} + \cdots + a_{n-1} z + a_n \). The updated state vector \( x = T \vec{x} \) transforms the system (previously given by (10)) into controllable canonical form, as,

\[
\vec{x}(k+1) = \vec{A} \vec{x}(k) + \vec{B} u(k)
\]

where the following is verified,

\[
\vec{A} = T^{-1} AT = \begin{bmatrix}
0 & 1 & 0 & \cdots & 0 \\
0 & 0 & 1 & \cdots & 0 \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
0 & 0 & 0 & \cdots & 1 \\
-a_k & -a_{k-1} & -a_{k-2} & \cdots & -a_1
\end{bmatrix}
\]

and,

\[
\vec{B} = T^{-1} B = \begin{bmatrix}
0 \\
0 \\
1
\end{bmatrix}
\]

Firstly, it is necessary to calculate \( \vec{K} \) so that \( u(k) = -\vec{K} \vec{x}(k) \) can place the poles in the desired locations. The eigenvalues will not be changed under similar transformation. In addition, \( u(k) = -\vec{K} T^{-1} x(k) \) also places the poles in the desired locations. If poles are placed at \( z_1, z_2, \ldots, z_n \) the characteristic equation can be written as,

\[
(z-z_1)(z-z_2)\ldots(z-z_n) = 0
\]

or, \( z^n + a_1 z^{n-1} + \cdots + a_{n-1} z + a_n = 0 \)

(16)

the controllable \((\vec{A}, \vec{B})\) can be located in,

\[
\vec{A} - \vec{B} \vec{K} = \begin{bmatrix}
0 & 1 & 0 & \cdots & 0 \\
0 & 0 & 1 & \cdots & 0 \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
0 & 0 & 0 & \cdots & 1 \\
-(a_k - k_1) & -(a_{k-1} - k_2) & \cdots & -(a_1 - k_n)
\end{bmatrix}
\]
the original and canonical form has a characteristic equation as: \(|zI-A|=z^n+a_1 z^{n-1}+\ldots+a_n=0\) while the characteristic equation of thier closed loop with \(u = -K \bar{x}\),

\[
z^n+(a_1 +K_n) z^{n-1}+(a_2 +K_{n-1}) z^{n-2}+\ldots+(an+K_1 )= 0
\]

from comparing (16) and (17), results,

\[
k_n = a_1 - a_1, K_{n-1} = a_2 - a_2, \ K_1 = a_n - an
\]

to find the actual gain matrix \(K = -K T^{-1}\), should be compute the transformation matrix \(T\), where \(\bar{K} = [K_1, K_2, \ldots, K_n]\).

### 4. RESULTS AND DISCUSSIONS

Firstly, the transfer function of the DC motor \(G_m(s)\) was transfed to state space representation (controllable canonical form), where the matrices of the state space. MATLAB/SIMULINK (R2015a) was used to finalize the simulation; it was used to demonstrate the robustness property of state feedback controller. Here, second order system is considered, which means that states of the system will reach the equilibrium in infinite time.

\[
A = \begin{bmatrix} 0 & 1 \\ -60.34 & -28.58 \end{bmatrix}; B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}; C = \begin{bmatrix} 20 & 30 \\ 0 & 0 \end{bmatrix}; D = \begin{bmatrix} 0 \end{bmatrix}
\]

The initial state was applied into the system is \(X(0)=[1 \ 0.5]^T\) and the estimated state feedback gain matrix \(K=[5.91 \ 0.42]\). First, the response for system without disturbance using state feedback controller is observed, both states will reach to the zero in infinite time as shown in Figures 4 and 5. In next step, a sinusoidal disturbance is introduced; it was shown that also both states will be reach to the zero in infinite time with very small oscillated as shown in Figures 6 and 7. State feedback control presented an acceptable response with stable behavior.

![Figure 4. Showing state X1 without any disturbance](image-url)

![Figure 5. Showing state X2 without any disturbance](image-url)

![Figure 6. Showing state X1 with the disturbance](image-url)

![Figure 7. Showing state X2 with the disturbance](image-url)
5. CONCLUSION
An analysis was proposed to evaluate the stability and performance of speed control in DC motor. State-feedback control technique was used with and without disturbance. The proposed control offered higher stability and performance in the response of the system in both cases. Therefore, this technique can be used to tackle the stability issue of speed control in DC motor.

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