Reservoir computing based on a silicon microring and time multiplexing for binary and analog operations

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Photonic implementations of reservoir computing (RC) promise to reach ultra-high bandwidth of operation with moderate training efforts. Several optoelectronic demonstrations reported state of the art performances for hard tasks as speech recognition, object classification and time series prediction. Scaling these systems in space and time faces challenges in control complexity, size and power demand, which can be relieved by integrated optical solutions. Silicon photonics can be the disruptive technology to achieve this goal. However, the experimental demonstrations have been so far focused on spatially distributed reservoirs, where the massive use of splitters/combiners and the interconnection loss limits the number of nodes. Here, we propose and validate an all optical RC scheme based on a silicon microring (MR) and time multiplexing. The input layer is encoded in the intensity of a pump beam, which is nonlinearly transferred to the free carrier concentration in the MR and imprinted on a secondary probe. We harness the free carrier dynamics to create a chain-like reservoir topology with 50 virtual nodes. We give proof of concept demonstrations of RC by solving two nontrivial tasks: the delayed XOR and the classification of Iris flowers. This forms the basic building block from which larger hybrid spatio-temporal reservoirs with thousands of nodes can be realized with a limited set of resources.

The last decade has seen a flourish of new machine learning (ML) methods and applications, sometimes surpassing the human's capabilities in solving hard tasks such as object recognition12, playing board games3 or lipreading4. Among the different approaches, Reservoir Computing (RC) has attracted growing interests due to its trade-off between performance and training complexity5. RC is a machine learning paradigm inspired by Recurrent Neural Networks (RNN) where a set of input stimuli triggers the nonlinear dynamics of a network of thousands of nodes, typically sparsely connected by fixed random weights6. The reservoir processes the information and maps the original input space into one of increased dimension, thus mimicking the sequence of nonlinear transformations of feed forward neural networks. In contrast with these, only the nodes in the readout layer are trained, while the network separability is guaranteed by the highly nonlinear dynamics of the reservoir. The training process is thus reduced to a linear combination of the output states of the reservoir, which can be implemented with minimal computational resources. At the heart of RC lies the fact that loose conditions on the topology of the reservoir are required for operation6, which find realization in a variety of physical systems. Among these, photonic RC promises to be the ideal platform for hardware acceleration, due to an ultra-high bandwidth of operation and ease of implementation8–11. Excellent demonstrations exist, which fall into two distinct categories: spatial and delayed-node reservoirs. The first has a close analogy with RNN, in which nodes are spatially distributed and can be physically interconnected, as in the network of Semiconductor Optical Amplifiers proposed in10, or can be software-connected, as the pixels of the spatial light modulator in13. Delayed node reservoirs use instead a single physical node for computation. Here, the nodes are virtual and multiplexed in time along an optical delay loop12. The network connectivity is given by the inertia of the system9, or by asynchronously sampling the readout nodes with respect to the time of injection of the inputs8,14. Implementations often use optoelectronic delay loops embedding nonlinear elements as Mach Zehnders or phase modulators9, DFB lasers15, VCSELs16 or photodetectors8. Being built from off-the-shelf optics and electronics, these systems operate at GHz speed and possess thousands of nodes. State of the art performances have been demonstrated on several benchmarking tests, as chaotic time series prediction, nonlinear channel equalization and speech
recognition. However, to satisfy the growing demand of more challenging tasks, the number of virtual nodes and their interconnection complexity is foreseen to increase over the next years. Scaling these parameters with bulk optoelectronic solutions will soon become unpractical for both spatial and delay-loop architectures. This is why numerous schemes based on integrated optics have been proposed, and some of them experimentally demonstrated. Silicon photonics is the ideal platform for very large scale integration, offering the possibility to fabricate hundreds of individually addressable and reconfigurable optical elements in few cm$^2$.[17] While coherent feed-forward neural networks have been recently reported[18, 19], the number of experimental demonstrations of RC based on silicon photonics still remain very limited[15, 20, 21]. Most of the proposed schemes focus on passive spatially distributed reservoirs made by small matrices of waveguides[20, 22], photonic crystal cavities[23] or ring resonators[24–26]. The fading memory of these systems is given by the delay lines which connect the nodes, or by the photon lifetime of the cavities. This memory spans from few ps to some ns. The nonlinearity is typically provided by the use of square law photodetectors, except for the theoretical works[24–26], where it is given by the nonlinear response of a MR. The scale of the reservoir is limited by the loss of the delay lines and by the repeated use of splitters (coherent combining) which create the connectivity of the network[27]. The integration of single nodes with delayed feedback eliminates the interconnection problem, but also faces challenges, since lossy delay loops of the order of few ns are required to store hundreds of virtual nodes with ps separation[25, 26]. It is natural to seek the use of hybrid spatio-temporal architectures as an optimal trade-off solution. These may adopt a small scale spatial topology with sparse connectivity, where each physical node can accommodate few hundreds of time multiplexed virtual nodes, similar to what is suggested in[28] and recently demonstrated on a silica chip[29]. It is worth noting that there are other approaches to increase the dimensionality of the network. Indeed, the exploitation of other degrees of freedom have been proposed, such as polarization and the longitudinal modes of a Fabry Perot cavity[26, 30].

In this work, we propose and experimentally validate a silicon MR and time multiplexing as a single physical node. The input space is encoded in time bins of different light intensity, which are injected in the device. The time bin duration is of the same order of the response of the nonlinear node, which triggers a transient state in the free carrier population. The carrier dynamics defines the connections between the virtual nodes. Specifically, in contrast to the systems shown in ref. [24–26], we adopt a scheme in which the input information is nonlinearly transferred from a pump to a weak continuous wave (CW) probe laser inside the MR. This is achieved by generating carriers through Two Photon Absorption (TPA) and then by imprinting their signature on the probe intensity by Free Carrier Dispersion (FCD), which shifts the resonance frequency of the cavity. The system does not require active materials and does not rely on photodetection to induce nonlinearities, being these naturally provided by TPA. The strength of information transfer is two orders of magnitude higher than the one mediated by Kerr, and occurs at modest input power thanks to the light enhancement inside the MR (see supplementary material). The reservoir operates at the rather slow timescale of 45 ns ($\sim$ 20 MHz), which is due to the unusually long carrier lifetime in our device. However, silicon waveguides with sub-ns carrier lifetimes are standard components of large scale photonic circuits[31, 32], and the use of carrier depletion modulators could further reduce this value to only tens of ps[33], closing the gap with the response time of laser cavities operating below threshold[35].

We experimentally demonstrate the RC capabilities with both binary and analog input signals. The binary task we address is the 1-bit delayed XOR, where we achieved a minimum detectable Bit Error Rate (BER) of $1.4 \times 10^{-4}$ for bitrates up to 30 MHz. The analog task we tackled is the classification of the Iris dataset[34], which yielded (99.3 $\pm$ 0.2)% accuracy at a rate of 0.38 MHz. We experimentally and theoretically show that the reservoir achieves its maximum performance when the carrier and the temperature dynamics slightly mix together, which occurs at the transition edge between a stable and a self-pulsing regime[35]. Finally, we discuss how to scale the presented scheme, showing that GHz operation with hundreds of thousands of nodes can be possible with limited resources.

**Principle of operation**

The architecture implements a single MR in the Add-Drop configuration as a reservoir, in which virtual nodes are defined by time multiplexing[36]. The way we construct and process the input and output layers is schematically shown in Fig. 1. The input signal $u(t)$, which can be a binary bit-sequence or of analog nature, is encoded in the intensity of a pump laser which is resonantly coupled to the input port of the MR. In contrast with common components of large scale photonic circuits[31, 32], and the use of carrier depletion modulators could further reduce ally long carrier lifetime in our device. However, silicon waveguides with sub-ns carrier lifetimes are standard components of large scale photonic circuits[31, 32], and the use of carrier depletion modulators could further reduce this value to only tens of ps[33], closing the gap with the response time of laser cavities operating below threshold[35]. We experimentally demonstrate the RC capabilities with both binary and analog input signals. The binary task we address is the 1-bit delayed XOR, where we achieved a minimum detectable Bit Error Rate (BER) of $1.4 \times 10^{-4}$ for bitrates up to 30 MHz. The analog task we tackled is the classification of the Iris dataset[34], which yielded (99.3 $\pm$ 0.2)% accuracy at a rate of 0.38 MHz. We experimentally and theoretically show that the reservoir achieves its maximum performance when the carrier and the temperature dynamics slightly mix together, which occurs at the transition edge between a stable and a self-pulsing regime[35]. Finally, we discuss how to scale the presented scheme, showing that GHz operation with hundreds of thousands of nodes can be possible with limited resources.

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The pump wavelength $\lambda_p$ is set with a small detuning $\Delta \lambda_p$ with respect to one of the resonance orders $\lambda_{pr,0}$ (pump resonance) of the MR. A second probe laser, at a constant power $P_{pr} \ll P_p$, is injected into the same port, and is tuned at a wavelength $\lambda_{pr} = \lambda_{pr,0} + \Delta \lambda_{pr}$, with a detuning $\Delta \lambda_{pr}$ with respect to the probe resonance wavelength $\lambda_{pr,0}$. We used $|\lambda_{pr,0} - \lambda_{pr}| = FSR$, where FSR is the Free Spectral Range of the MR. In the rest of this paper, we refer to $\lambda_{pr}(\lambda_{pr})$ as the “cold” pump(probe) resonance, that is the resonance wavelength of the MR in the linear operation regime, where all the nonlinear effects, which might affect the resonance frequency, are neglected. As a consequence of light confinement in the MR, the pump intensity builds up, and TPA promotes neglected carriers from the valence to the conduction band. This changes the refractive index of the material through FCD, inducing a rigid blue shift of all the eigenfrequencies of the MR. Concurrently, the round-trip loss is increased by Free Carrier Absorption (FCA). Since $u$ varies in time, the magnitude of the FCD shift changes as well, and its dynamics is imprinted on the probe laser intensity at the output of the MR. The latter incoherently transfers the input information from the pump to the probe beam. It is worth to note that the FCD shift caused by TPA is two orders of magnitude higher than the Kerr shift (see supplementary material), and acts as an effective intensity induced nonlinearity. The carrier lifetime $\tau_c$ is much smaller than the thermal constant $\tau_0$ of the MR. Therefore, when $\Delta T \sim \tau_c$, the MR temperature variations $\Delta T$ cannot follow the temporal profile of the carrier concentration. Self heating effects due to carrier relaxation are smoothed to yield a steady state value $\Delta T$. In this regime, the MR temperature does not participate to the reservoir dynamics, and only changes the effective detuning $\Delta \lambda_{pr}$ of the pump(probe) resonance. However, as discussed in "Enhancing the reservoir performance by mixing thermal and free carrier dynamics" section, this holds only at low input power. When the average power is raised above a certain threshold, the MR starts to self-pulse, and the temperature dynamics impacts the processing capabilities of the nodes.

We can get an insight on the internal structure of the reservoir by assuming small perturbations of the input power $u(t)$ with respect to a reference value $u(0)$. Here, small means that the corresponding free carrier change $\Delta N = \Delta N_0$ around the reference value $\Delta N_0$ induces variations of the transmitted pump/probe intensity which are linear with $\Delta N$. As derived in the supplementary material, within this approximation the probe power $u_{pr}$ at the Drop port of the resonator is given by:

$$u_{pr}(t) = c_0 + c_1 \int_{-\infty}^{t} e^{-\left(\frac{\xi - t}{\tau_m}\right)} u^2(\xi) d\xi + c_2 \int_{-\infty}^{t} e^{-\left(\frac{\xi - t}{\tau_c}\right)} u^2(\xi) u_{pr}(\xi) d\xi,$$

where the definitions of $c_0, c_1$ and $c_2$ are provided in the supplementary material. The first contribution to the virtual node state at time $t$ is quadratic in the pump power $u$, and depends on the past inputs with weights that exponentially decrease with time. This short term memory is of the order of $\sim 3 \tau_c$, i.e., the time required by free carriers to reach a steady state after an abrupt change of the pump power. The memory of this system is thus intrinsically nonlinear. This is because the input information $\mathbf{x}^{(n)}$ is instantaneously (fs scale) transferred to carriers through nonlinear absorption, temporarily processed from a slower (ns) dynamics, and subsequently imprinted to the output probe. Similarly to what is done in $\ref{1}$, one can approximate the integral in the first term with a discrete sum, and find the recursive virtual node relation $u_{pr}(t_{n+1}) = \Delta c_1 \sum_{k=0}^{m} (\eta^k u(t_{n,k-\xi})) + \eta^k u_{pr}(t_{n,k-\xi})$, where $\eta = e^{-\left(\tau_m / \tau_c\right)}$ (for simplicity, the second term in Eq. (1) has been neglected, but this does not alter our conclusions). This highlights the type of connectivity between the virtual nodes of the reservoir, which are organized in a chain-like topology: node $u_{pr}(t_{n,i})$ is coupled with its adjacent $u_{pr}(t_{n,i-1})$ with a coupling strength $\eta$. The latter exponentially decreases with the time separation, so the number of coupled nodes depends on $\Delta$. It
has been shown that an optimal value for $\Delta$ is of the order of $\sim \tau / S$, where $\tau$ is the characteristic time response of the nonlinear node.\textsuperscript{9,36} We choose $\Delta \sim \tau_c$ for our experiment, which is fast enough to prevent our device to reach a steady state. The second term in Eq. (1) is a nonlinear coupling between virtual nodes. This term arises from the the resonance shift induced by FCD (see supplementary material). The shift modifies the pump power circulating in the MR, which in turn affects the carrier generation rate. As a result, a recursive relation between these quantities is settled, for which the second term in Eq. (1) accounts for the leading term. When the change in $u_{pr}$ is no more linear with $\Delta N - \Delta N$ due to large FCD induced resonance shifts, Eq. (1) loses validity and the virtual node interaction becomes increasingly complex. The general structure of the network is however maintained, with TPA and inter-node coupling providing nonlinearity, while carrier recombination a short term memory to the reservoir. Virtual nodes $u_{pr}(t_n)$ are sampled at the Drop port synchronously with the input, and arranged into a state matrix $X = [u_{pr}^{(1)}, \ldots, u_{pr}^{(M)}]^T$, where $u_{pr}^{(k)}$ is the column vector collecting the $N_v$ virtual nodes corresponding to the $k$th input sample $x^{(k)}$. The action of the reservoir is to project the initial set of predictors $x^{(k)}$ with corresponding observables $y^{(k)}$ (in general, a Q-dimensional vector) to a higher dimensional space $x^{(k)} \rightarrow u_{pr}^{(k)}$ where they ideally should be linearly separable. Then, the aim is to find a $(N_v \times Q)$ weight matrix $W_{out}$ which realizes $Y = X W_{out}$, in which the observables are arranged in the $M \times Q$ matrix Y. We accomplish this task by regularized least squares (Ridge regression), where the regularization parameter $\lambda$ is determined by a 5-fold cross validation.\textsuperscript{94} The output of this procedure is a matrix $W_{out}$ which minimizes the regularized least square error $\sum_{i=1}^{M} ||(Y - W_{out}X)||^2 + \lambda^2 ||W_{out}||^2$. In case of supervised learning, as we deal in this paper, $y^{(k)}$ is a Q-dimensional binary variable, with 1s identifying the assignment category of $x^{(k)}$ and 0s elsewhere. Given $\tilde{y}^{(k)}$ and $y^s$, the way decisions arhandled depends on the task, and will be treated separately in “Binary input: 1-bit delayed XOR” and “Analog input: Iris species recognition” sections.

**Experimental realization**

Our experimental apparatus is sketched in Fig. 2. The pump is a C-band, CW tunable laser (Pure Photonics) which is intensity modulated by an electro-optic IQ modulator (IxBlue MXIQ-LN-30) to realize the desired input pump waveform $u(t)$. The modulator is driven by a 65 Gs Arbitrary Waveform Generator (AWG) from Keysight, whose output is amplified by a high bandwidth amplification stage (IxBlue DR-AN-28-MO), providing the necessary voltage swing of $V_{p} \sim 7$ V to exploit the full dynamic range of the modulator. In order to claim that the nonlinear transformation on the input samples is solely coming from the MR, we did a pre-compensation of the signal out of the AWG, which eliminates the $\cos^2$ dependence of the modulator intensity response with the applied voltage. A tap of 10% is placed at the output of the modulator to monitor the input pump, which is detected by
Figure 3. (a) Examples of waveforms processed during the XOR task. The pump laser driving the input port of the MR is shown in black, while the pump and probe outputs from the Drop port are respectively shown in red and blue. (b) Bit Error Rate (BER) as a function of the bitrate for the 1-bit delayed XOR task. Black dots use predictors sampled from the pump and the probe traces at the Drop port of the MR. In these three cases, the average pump power is set to 3 dBm. (c) Bit Error Rate as a function of the average pump power for a fixed bitrate of 20 Mbps. The insets show details of the probe waveform at the pump powers −10 dBm and 4 dBm.

A fast photodiode (Thorlabs DXM20AF). The pump is amplified to a fixed level of 20 dBm by an Erbium Doped Optical Amplifier (EDFA, IPG Photonics) and the power regulated by an electronic Variable Optical Attenuator (VIAVI mVOA-C1). A second CW probe laser (Pure Photonics) is combined with the pump before being injected into the input port of the MR using a single mode fiber and a Grating Coupler (~3.5 dB loss). The MR under test has a racetrack shape, with a radius of 7 μm and a waveguide cross section of 450 nm × 220 nm. Two bus waveguides are coupled to the straight sections of the MR, with a gap of 250 nm and a coupling length of 3 μm. The device is described in detail in Ref. 37. From the low-power transmission spectra recorded at the Through port, we extracted an intrinsic quality factor (Q) of Q = 1.11(8) × 10^5 and a loaded Q of Q_L = 6.5(2) × 10^5. We use two adjacent resonance orders to resonantly couple the pump and probe laser, which have respectively cold resonance wavelengths of ~1549 nm and ~1538 nm. Light at the output of the Drop port is amplified by a second EDFA (Thorlabs), and a tunable band-pass filter (0.8 nm bandwidth) removes the spontaneous emission and directs the probe or the pump laser to the output photodiode (Thorlabs D400FC, 1 GHz bandwidth). A 4 × 40 Gs oscilloscope (LeCroy SDA 816Zi-A) records the input pump waveform u(t) and the output probe waveform tpr(t). Virtual nodes are sampled from tpr(t) at times tk and queued to form the state matrix X. Training and validation are performed off-line using Matlab.

Binary input: 1-bit delayed XOR. The first task we tested is the 1-bit delayed XOR20. Given the virtual node vector tk at time tk, the goal is to predict the result of the XOR operation between the bits x(k) and x(k−1).

The input variable can assume two values, 1 (full transmission of the modulator) and 0 (full extinction). In this task, we use Nv = 3 virtual nodes, and the connectivity mask is simply a 3 × 1 column vector of 1s. This implies that no mask is applied to the input data, so that ut(tk−τc) = x(k)ut(tk−τc). We do not aim to use this task as a benchmark, but to give proof of concept demonstration of the architecture operation, which involves: the nonlinear transformation of the inputs, the presence of a fading memory, and the ability to deal with binary inputs. In this experiment, we fix the average power of the pump at the input to 3 dBm, which is sufficient to trigger TPA and carrier generation, and its detuning to Δc = 60 pm. The pump intensity is modulated with ~18 dB of extinction, and the input is a Pseudo Random Binary Sequence (PRBS) of bitrate B, which we varied from 10 Mbps to 80 Mbps. The probe power is set to Ppr = −3 dBm, which is sufficient low to not alter the resonance shift imparted by the pump, and its detuning to Δc = 60 pm. An example of waveforms at the input and output of the MR for a bitrate of 30 Mbps are shown in Fig. 3(a). Whenever the input pump changes from a low to a high state, a transient exponential decay is observed at the Drop port, which is due to the blue shift of the resonance as a consequence of carrier generation and accumulation. The cold cavity detuning ΔLpr = 60 pm is increased by FCD, determining a decrease of the transmittance, which also occurs for the probe output. The opposite trend is observed, in the probe trace, during the transition from a high to a low state. Here, carrier recombines and the detuning ΔLpr = 60 pm decreases, pulling the resonance back to the cold position. All the transient phenomena occur at the characteristic timescale of τc = 45 ns, i.e., the value of the carrier lifetime we measured in one of our previous works24. Virtual nodes are obtained by sampling these traces at 10 Gbps, smoothing them with a moving average filter (10 points), and downsampling them at times Δ = (N, B)^−1. After smoothing, the Signal to Noise ratio (SNR) increases from 18 dB (from the raw data acquisition) to ~20 dB. The procedure for the estimation of the SNR is detailed in the supplementary material. Figure 3(b) shows the Bit Error Rate (BER) as a function of the bitrate for different predictor matrices X, whose entries are respectively populated by sampling the virtual node values from the input pump intensity (black), the output pump power (red) and the output probe power (blue). To
extract the BER, 6500 bits are used for training and 3500 for validation. Errorbars are obtained by partitioning the validation set into 5 non-overlapping batches, over which the BER is evaluated. The error is estimated as the standard deviation over the different batches. The output of the linear classifier $Y$ is digitized by applying a threshold, which optimizes the BER at each bitrate. The XOR task is never solved by sampling virtual nodes from the bare input pump. The average BER is $\sim 30\%$ for all the bitrates. This agrees with the fact that the task is not linearly separable and requires at least one bit of memory to be performed.

Virtual nodes sampled from the pump at the output of the Drop port improve the BER, which is however still bounded above $\sim 5\%$. The reason behind this is that bits which are zero do not carry optical power, so these virtual nodes are sampled from the background noise. This issue is solved by using the probe signal. Indeed, error free operation is achieved for bitrates lower than 25 Mbps. Since we use 700 bits for each partition, error free means that the actual BER is lower than $1.4 \times 10^{-3}$. At higher rates, carriers are no more able to react sufficiently fast to follow the pump power variations, so the BER increases. The ability to solve the delayed XOR demonstrates the presence of memory and nonlinearity in the reservoir. This also illustrates that the use of a probe beam is beneficial for tasks where the input is binary and with full modulation. It helps to improve the separability of the reservoir\(^25\). To investigate the influence of the input power on the BER, we fixed the bitrate to 20 Mbps, and we changed the average input power of the pump $P_p$. The calculated BER is shown in Fig. 3(c). The error rate is almost power-insensitive and equal to $\sim 25\%$ for $P_p < -4$ dBm, while it drops below 1% at $P_p = 0$ dBm. At $P_p > 2$ dBm, error-free operation is achieved. The low and high power insets shown in Fig. 3(c) explain why the BER improves by increasing power. At $P_p = -10$ dBm, few carriers are generated, so the probe is weakly perturbed from its original CW state and virtual nodes acquire a noisy flat distribution of values. At $P_p = 4$ dBm, the FCD shift is source of more variability in the virtual nodes states, improving the input separability of the reservoir. We also averaged several traces at low power in order to compare the performance at the same SNR of the ones at high power, but we only observed a minor improvement of the BER. This confirms that the poor performance measured at low power is due to the reduced virtual node variability.

**Analog input: Iris species recognition.** The second task we addressed is the classification of the Iris flowers, a popular toy-dataset in the field of machine learning\(^4\), and being so, not intended to be used as a benchmark against other reservoir systems. Here, the goal is to classify a given Iris flower into one of the three possible subspecies: *Setosa*, *Versicolor* and *Virginica*. The classification is based on four real inputs $x$, physically corresponding to the length and width of the petals and sepals of the flower. All the four inputs are required to solve the task, since the flowers can not be linearly classified on the basis of a single feature. Moreover, even by using all the four inputs, only one species (*Setosa*) is linearly separable from the others, making the task non-trivial. As described in “Principle of operation” section, the dimension of the original input space is increased from 4 to $N_v$ by implementing the transformation $x \rightarrow W_n x$, where the connectivity matrix $W_n$ has dimension $N_v \times 4$. An offset is applied to the transformed input to remove the negative values, and the result is scaled to reach the desired target average power $P_p$. We tested different numbers of virtual nodes $N_v = \{10, 25, 50\}$, and two values of time separation $\Delta = (25, 50)$ ns. Each flower sample is sequentially encoded in the pump intensity $u(t)$ and injected into the input port of the MR. Different flowers are separated by a delay of $\delta = 100$ ns, during which the pump power is turned off to quench the carrier dynamics. This avoids undesired crosstalk of information between neighbouring flowers, resetting the MR to the same initial conditions after each sample injection. The original dataset contains 150 flowers, with an equal number of representatives of each class. Each instance injected into the chip is randomly extracted from the dataset. Figure 4(a) (top panel) shows an example of pump waveform at the input of the MR for three flower instances of different subspecies. Each is made by 50 steps, which corresponds to the virtual nodes. The low speed of operation allows to use the full resolution of the digital to analog converter of the AWG (8 bit), imprinting on the optical power trace the fine details of each flower sample. The associated probe waveform, after being processed by the MR reservoir, is shown in Fig. 4(a) (bottom panel). With respect to the XOR task, where the input is binary, the multilevel excitation imparts a richer dynamics on the output probe, which results in an enhanced variability between the virtual nodes. The reservoir response to different flower samples is represented in the maps of Fig. 4(b), which shows the intensities of the 50 virtual nodes for 189 flower instances (vertically stacked). In Fig. 4(c) we report the classification rate for 20 Mbps and 40 Mbps as a function of the average input power. Categories are assigned by training multiple linear classifiers, one for each subspecies, and decisions are made on the basis of a winner takes all scheme\(^9\). The best performance is obtained for 20 Mbps and a pump power of $P_p = 7$ dBm, yielding a classification rate of $(99.3 \pm 0.2\%)$. In comparison, the classification rate obtained by sampling the virtual nodes from the input pump is below 87%. This value is slightly above the theoretical limit of 84.66%, obtained by directly feeding the input predictor matrix $W_n x_0$ into a linear classifier. This is probably due to some residual nonlinear distortion in the electro-optic conversion. The rate of classification obtained by a single MR exceeds the accuracy achieved by a more complex integrated system (three layered feed forward neural network)\(^{10}\), and has competitive performance with respect to software based classification algorithms\(^{26}\) or compared to a complex-valued perceptron, which has been recently implemented on a coherent photonic processor\(^{19}\). The classification rate in Fig. 4(c) increases from low to high power, reaches a maximum at 7 dBm and then decreases for higher powers. We can understand this trend by observing the virtual node intensity in the maps of Fig. 4(b). At low powers ($P_p = 4$ dBm in Fig. 4b), the MR reservoir shows poor separability of the inputs, as witnessed by the quite flat virtual node intensity distribution observed both within the same flower (horizontal lines) and between different subspecies (vertical lines). As discussed for the XOR task, this is related to the weak perturbations imprinted on the CW probe from the pump intensity at low powers. At the highest classification rate of $P_p = 7$ dBm (Fig. 4b), the virtual node distribution is richer, with a relative variation that can exceed 70% (see Fig. 4b at $P_p = 7$ dBm). We also observe the creation of two bands, where the virtual node intensity is around the 35% of its maximum
value. As discussed in “Enhancing the reservoir performance by mixing thermal and free carrier dynamics” section, these form as a consequence of the interplay between thermal and free carrier dispersion. At high power ($P_p = 9$ dBm in Fig. 4b), multiple bands of low transmittivity are formed, which lack synchronization with the rate of flower injection. Within the bands the MR is off resonance, hence the information cannot be efficiently imprinted from the pump to the probe, effectively “burning” these virtual nodes from the reservoir. This explains the drop in the classification accuracy at high powers.

The net flower classification rate can be calculated as $(N_v \Delta + \delta)^{-1}$, which for $N_v = 50$ and $\Delta = 50$ ns, i.e., the configuration showing the best accuracy, is 0.38 MHz. We tried to scale down to $N_v = 25$ and $N_v = 10$ in order to improve the speed of operation, but as shown by the confusion charts in Fig. 4(d), the classification accuracy drops to $(93.6 \pm 0.3\%)$ for $N_v = 25$ and $(89.2 \pm 0.2\%)$ for $N_v = 10$. We did not observe any significant improvement by scaling up to $N_v = 100$.

**Enhancing the reservoir performance by mixing thermal and free carrier dynamics.** In order to explain the behavior of the classification rate as a function of the input pump power in Fig. 4(c), we performed numerical simulations. They are based on the theoretical model of\(^3\). Specifically, we computed the time evolution of the complex field in the MR, including TPA, FCA, FCD and the thermo optic dispersion (TOE). Whenever possible, the parameters are taken from the experiment. A more comprehensive description of the model

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Figure 4. (a) Examples of waveforms of the input pump (top panel, in black) and of the probe at the output of the MR (bottom panel, in blue) for $N_v = 50$ and a bitrate of 20 Mbps. Different background colours highlight the subspecies of the flower. Virtual nodes sampled from the probe trace are indicated with red dots on the central band. (b) Maps of the (normalized) intensity of the different virtual nodes ($N_v = 50$, bitrate 20 Mbps) sampled from the output probe, acquired at the pump powers of 4 dBm (left), 7 dBm (center), and 9 dBm (right). These are 189 flower samples vertically stacked in each map. Even if they are randomly injected at the input port during the training and test phase, they are shown grouped together in the three subspecies, as indicated by the labels on the left. This highlights the distinction between the classes. (c) Classification rate as a function of the average input power of the pump for $N_v = 50$ and bitrates of 20 Mbps (left) and 40 Mbps (right). Black scatters use virtual nodes sampled from the output probe while red scatters from the input pump. The dashed blue line is the lower bound in the classification rate obtained by feeding the input samples into a linear classifier, without electro-optic conversion. (d) Confusion charts for a MR reservoir which uses 10 (left), 25 (center), and 50 (right) virtual nodes. The bitrate is 20 Mbps.
can be found in\textsuperscript{37}. We fix the number of virtual nodes to 50, the bit rate to 20 MHz and the quenching time to $\delta = 100$ ns.

The top panel in Fig. 5(a) shows the simulated classification rate as a function of the input power, estimated from the whole Iris dataset (150 flowers). We add white noise to the simulated output of the MR to set the SNR to 18 dB, which is comparable to the one of the experiment (the latter monotonically decreases from $\sim 25$ dB at 2 dBm of input Pump power to $\sim 17$ dB at 9 dBm, see supplementary material for details). Each point is the result of an average over 1000 realizations. We notice a very good agreement with the experimental data in Fig. 4(c), with a maximum of classification occurring around 7 dBm.

We investigate the origin of this trend starting from the color map reported in the bottom panel of Fig. 5(a). Here, for each input power, we calculate the probability that a virtual node is sampled at the probe resonance detuning $\Delta \lambda$ from the cold cavity condition. At low power, all virtual nodes are sampled around the cold resonance detuning, which in our case lies at $\Delta \lambda = 60$ pm. As we raise the input power up to about 5 dBm, FCD shifts the resonance frequency towards the blue, further increasing the initial detuning. Starting from 6 dBm, we observe that the variance increases, and that there is a small probability to sample virtual nodes at negative detunings. For $P_p > 6$ dBm, the distribution

**Figure 5.** (a) Top: numerical simulation of the Iris dataset classification rate as a function of the input power. Bottom: probability distribution of the virtual node detuning $\Delta \lambda$ as function of the input pump power. (b) Simulated probe power at the Drop port of the MR (top), temperature variation (middle) and free carrier concentration for $P_p = 9$ dBm. The red dashed lines mark the injection times of three different flower samples. The color code indicates the instantaneous detuning of the probe, whose relation with the Drop intensity is shown in panel (c). (c) Normalized intensity at the Drop port of the MR as a function of wavelength. The dashed line marks the wavelength of the probe laser. The color code is used to label the instantaneous detuning of the time traces in panel (b).
is bimodal, i.e., nodes are concentrated around two bands: a narrow one at positive $\Delta \lambda$ and a broad one at negative $\Delta \lambda$. This is a signature that the temporal evolution is not only related to free carriers, where the temperature acts as a constant background. In fact, at these powers, we are entering a regime where carriers and temperature dynamics mix together. This is shown in the panels of Fig. 5(b), which refer to $P_p = 9$ dBm. Here we report, as a function of time, the output power of the probe (top), the temperature difference between the MR and its surroundings (middle), and the free carrier concentration (bottom) for three consecutive flower samples (the injection times are marked with red dashed lines). The color code indicates the instantaneous detuning of the probe, whose relation with the Drop intensity is shown in Fig. 5(c). When a flower sample is injected, the temperature of the MR increases, but at low powers TOE is counteracted by FCD. At high power TOE prevails, and the wavelength detuning of the cavity can eventually become negative. When this occurs, a positive feedback is established between the decrease of the carrier concentration and the decrease of MR energy. This corresponds to the transition from the high power stability branch of the carrier bistability curve to the one at low power41. After the transition, the MR lies off resonance35. The detuning is now negative due to the residual thermo optic shift. This originates the bands of low transmittivity in Fig. 4(b) and in Fig. 5(b). Virtual nodes sampled within these bands form the second broad peak in the probability distribution in Fig. 5(a). As the MR cools down, the resonance moves towards the pump(probe) wavelength, gradually increasing the probe signal. A transition from the low power stability branch of the carrier bistability curve to the one at high power restores the initial conditions, so that virtual nodes are no more sampled within the band. This interplay of thermal and free carrier effects would generate cavity self-pulsing in case of CW input powers35. It turns out that, for a limited range of powers centered around 7 dBm, the presence of the bands increases the classification rate. This finds explanation in the enhanced variability that the virtual nodes values assume. Indeed, in this regime, they efficiently sample the probe resonance. Moreover, quenching the MR for $\delta = 100$ ns allows to reset the initial conditions for the temperature and the carrier population between coupled nodes in the same time slot (see Fig. 4(b), $P_p = 7$ dBm). If the power is increased above 7 dBm, bands get wider in time and many of them form within the same flower sample. In these conditions, a large number of virtual nodes are sampled within bands, where the cavity lies off resonance and hence no information can be transferred from the pump to the probe beam. Furthermore, the quenching time is no more sufficient to reset the initial conditions, so as bands form at random times, turning the probe output to chaotic (see Fig. 4(b), $P_p = 9$ dBm)42.

Discussion

In the above sections, we demonstrated the use of a single integrated MR as a reservoir, in which the core computing power is provided by the complex coupled dynamics of free carriers, TPA and temperature. The overall power consumption is estimated to be around 1500 W, and is distributed as follows: 60 W for the Pump and Probe lasers, 5 W for the electrical amplifiers, 180 W for the AWG, 40 W for the optical amplifiers, 1000 W for the oscilloscope and 200 W for the laptop. This is comparable to the value of 1300 W reported in a recent work on a silica chip39, and is expected to not significantly differ from the one of more advanced photonic classifiers8,9,43, since most of the power consumption arises from the electronics used for data acquisition, control and post-processing, rather than from the optical components. The architecture is proof of concept and suffers from an unusually slow carrier recombination time. As such, it faces limitations in terms of speed, dimensionality, power consumption and performance, which are nevertheless not of fundamental origin. We now outline how to improve these metrics with modest technological effort. First, to increase the dimensionality, the MR can be used as a building block to form more advanced spatial topologies, i.e. matrices/arrays of MR. As an example, using resonators with a moderately high Q factor of $6.5 \times 10^4$, a network made by 10 MR can accommodate 500 virtual nodes and operates with 5 mW of power. Small sequences of coupled resonators have shown very complex dynamical behavior under thermal and free carriers nonlinearities44. This performance could be obtained with less virtual nodes, hence increasing the speed of operation. Additionally, a narrower cavity linewidth enhances the sensitivity of the reservoir to small resonance perturbations, decreasing the input power needed to trigger free carrier effects. Higher degrees of complexity and computational power could be realized by multiplexing several spatial inputs44 and by coherently combining them on chip using linear optical elements, such as arrays of Mach-Zehnder interferometers arranged in a universal scheme46. This hybrid spatio-temporal architecture combines a simple hardware implementation, typical of delayed nodes RC, with the compactness of a silicon photonic chip. Second, to increase the speed of operation and reduce the power consumption, the intrinsic time response of the RC can be improved by reducing the carrier lifetime. Indeed, our device shows a recombination time which is almost two orders of magnitude higher than the ones commonly reported in literature47. Several factors may hinder the recombination process, such as a small surface trap density or the presence of trap states located below the Fermi level of the semiconductor47. A prior analysis performed on the same device rules out the latter hypothesis37. We can then speculate that the long carrier lifetime is associated to a small trap density, which could correspond to a well passivated waveguide surface. It is possible to push the lifetime down to tens of ps by embedding carrier depletion modulators within the MR35. The aggregate processing speed can be also improved by adopting wavelength-division multiplexing48,49. This would require to use multiple pump lasers whose wavelengths are matched to the different resonance orders of the MR. Different virtual nodes can be encoded into distinct wavelengths and simultaneously injected into the reservoir. It is worth to note that this is not equivalent to operate several independent reservoirs in parallel. Indeed, since the carrier population interacts with all the optical channels, they become coupled (second term in Eq. (1))47, and additional virtual node interaction is expected from Cross Photon Absorption. In this sense, the number of Multiply-Accumulate (MAC) operations will not generally scale with the number of wavelengths.

Another aspect of concern is the memory capacity. Since our device lacks of a delay loop, the memory is provided by carrier relaxation, and is of short term. As shown in “Principle of operation” section, the input is
convoluted with a slow exponential decay, which means that the virtual node coupling only extends over the first few neighbours. We can anyway compensate the absence of a long-range coupling by encoding the memory over past samples in the input layer. Indeed, it has been shown that a delay loop reservoir whose feedback has been removed can still be effective in time prediction tasks, provided that memory over past samples is given at the input\textsuperscript{21,48}. To see how this can be implemented in our scheme, we consider the discrete time version of Eq. (1), and express the pump field as \( u(t_{n,i}) = \sum_{k=1}^{N} W_{ik} x_{k}^{(n)} \), which gives the following probe amplitude at the output layer:

\[
\begin{align*}
    u_{pr}(t_{n,i}) & \sim \sum_{k \neq q} e^{-\frac{k}{\tau}} W_{i-k,q} W_{i-k,q} r_{q,q} x_{q}^{(n)} + O(u_{pr}) \\
\end{align*}
\]

where the sums over \( q \) and \( q' \) run over all the components of the \( n \)th input sample, while \( r_{q,q} = 1 \) if \( q = q' \) and \( r_{q,q'} = 2 \) if \( q \neq q' \). This is equivalent to operate \( N \) sample and hold circuits, each applying a different mask \( W_{i} = \{W_{in} \} \) \((i = 1, N)\) where \( \{W_{in} \} \) denotes the \( j \)th column of \( W_{in} \) to separate inputs \( x_{j} \). The outputs of the \( N \) circuits are then multiplexed in the same input port to excite the nonlinear node. In time series prediction tasks, the \( x_{q}^{(n)} \) can be the values of the series \( i_{q}(t) \) sampled \( q \) bits ahead in time, i.e., \( x_{q}^{(n)} = i_{q}(n - q)T \), where \( q \) runs over all the past samples which are relevant to perform predictions. The approach unifies the concepts of reservoirs and extreme learning machines\textsuperscript{46}. Compared to delayed loop reservoirs, the overhead is that several delayed copies of the same input series and a combination stage are required. This is not of particular concern since in most of the cases an electro-optic conversion is involved to shape the input series from a CW optical input, so all the described pre-processing steps can be done in the electronic domain using a combination of delay lines and fan-in(out) circuits. An alternative strategy is to use different wavelength channels to encode the delayed copies, and to broadcast them into the same spatial mode using an on-chip wavelength multiplexer, as an Arrayed Waveguide Grating or a Mach Zehnder interleaver. As a last remark, we point that the presence of a delay loop may not always be desired. While it is certainly beneficial for tasks requiring a long term memory, in classification tasks this introduces crosstalk among different objects, which deteriorates the input separability.

Conclusions

In this work, we have experimentally shown a time multiplexed architecture which uses a single integrated MR as a substrate for RC. We encode the input layer in the temporal evolution of the intensity of a pump laser. When this is resonantly coupled to the MR, the information is transferred to a secondary probe laser, which is delayed copies, and to broadcast them into the same spatial mode using an on-chip wavelength multiplexer, as an Arrayed Waveguide Grating or a Mach Zehnder interleaver. As a last remark, we point that the presence of a delay loop may not always be desired. While it is certainly beneficial for tasks requiring a long term memory, in classification tasks this introduces crosstalk among different objects, which deteriorates the input separability.

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