Starbursts and torus evolution in AGN

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Abstract. Recent VLT SINFONI observations of the close environments (~ 30 pc) of nearby AGNs have shown that thick gas tori and starbursts with ages between 10 and 150 Myr are frequently found. By applying these observations to a previously established analytical model of clumpy accretion disks, we suggest an evolutionary sequence for starburst and AGN phases. Whereas the observed properties of the gas tell us about the current state of the torus, the starburst characteristics provide information on the history of the torus. In the suggested evolution, a torus passes through 3 different phases predetermined by an external mass accretion rate. Started by an initial, short, and massive gas infall, a turbulent and stellar wind-driven $Q \sim 1$ disk is formed in which the starburst proceeds. Once the supernovae explode the intercloud medium is removed, leaving a massive, geometrically thick, collisional disk with a decreasing, but still high-mass accretion rate. When the mass accretion rate has significantly decreased, the collisional torus becomes thin and transparent as the circumnuclear disk in the Galactic center of the Milky Way. Variations on this scenario are possible either when there is a second short and massive gas infall, in which case the torus may switch back into the starburst mode, or when there is no initial short massive gas infall. All observed tori up to now have been collisional and thick. The observations show that this phase can last more than 100 Myr. During this phase the decrease in the mass accretion rate within the torus is slow (a factor of 4 within 150 Myr). The collisional tori also form stars, but with an efficiency of about 10\% when compared to a turbulent disk.

Key words. Galaxies: active – Galaxies: nuclei – ISM: clouds – ISM: structure – ISM: kinematics and dynamics

1. Introduction

In the unification scheme for active galactic nuclei (AGN) the central massive black hole is surrounded by a geometrical thick gas and dust torus (see, e.g., Antonucci 1993). If the observer’s line-of-sight crosses the torus material, the AGN is entirely obscured from near-IR to soft X-rays and only visible at X-ray energies if the gas column density is not too high (Seyfert 2 galaxies). On the other hand, if the torus is oriented face-on with respect to the observer, the central engine is visible (Seyfert 1 galaxies). The spectral energy distributions (SEDs) of most quasars and AGN in Seyfert galaxies have a pronounced secondary peak in the mid-infrared (mid-IR) (e.g. Sanders et al. 1989; Elvis et al. 1994), which is interpreted as thermal emission by hot dust in the torus. The dust is heated by the primary optical/ultraviolet (UV) continuum radiation, and the torus extends from the dust sublimation radius outwards (Barvainis 1987).

The geometrical thickness of the torus in the gravitational potential of the galactic nucleus implies a vertical velocity dispersion of about 50-100 km s\textsuperscript{-1}. If one assumes that the disk is continuous, i.e. thermally supported, this corresponds to a temperature of $\sim 10^5$ K. Since this is beyond the dust sublimation temperature ($\sim 10^3$ K), thick tori have to be clumpy or must be supported by additional forces other than thermal pressure. Krolik & Begelman (1988) proposed a clumpy torus model where the clumps have supersonic velocities. Vollmer et al. (2004) and Beckert & Duschl (2004) elaborated this model in which clumpy tori form stars, but with an efficiency of about 10\% when compared to a turbulent disk. If and how efficient these clumpy tori form stars is an open question. The large majority of observational studies probed the nuclear star formation on scales of a few hundred parsecs (see, e.g., Sarzi et al. 2007, Asari et al. 2007, González Delgado & Cid Fernandes 2005, Cid Fernandes et al. 2004). These studies resulted in a general view that about 30\% - 50\% of the sample AGNs are associated with recent (ages less than a few 100 Myr) star formation on these scales. Thanks to the high spatial resolution of the near-infrared adaptive optics integral field spectrograph SINFONI, it has only recently become pos-
sible to study the environments of AGN on the 10 pc scale. Davies et al. (2007) analyzed star formation in the nuclei of nine Seyfert galaxies at spatial resolutions down to 0.085″. They found recent, but no longer active, starbursts in the central regions which occurred 10 - 300 Myr ago. Moreover, Hicks et al. (2008) were able to measure the rotation and dispersion velocity of the molecular gas in these galaxies using the 2.12 μm H2 (1-0)S(1) line. Surprisingly, all molecular gas tori have high velocity dispersions and are therefore geometrically thick.

In this article we compare the observations of Davies et al. (2007) and Hicks et al. (2008) with the expectations of analytical models of clumpy accretion disks developed in Vollmer & Beckert (2002, 2003) and Vollmer et al. (2004). In a first step, we test whether these models are able to describe observations. In a second step, these models allow us to investigate the scenario hypothesized by Davies et al. (2007) where sporadic, short-lived starbursts are due to short massive accretion events in the central region, followed by more quiescent phases until there is another episode of accretion. This scenario is corroborated by a closer look at the nucleus of NGC 3227 where Davies et al. (2006) found signs of a past starburst (∼ 40 Myr ago) and a presently quiescent gas torus with a Toomre parameter Q > 1.

2. The theory of clumpy gas disks

Within the framework of Vollmer & Beckert (2002, 2003) and Vollmer et al. (2004) clumpy accretion disks are divided into two categories: (i) turbulent and (ii) collisional disks. In case (i) the ISM is regarded as a single entity which changes phase (molecular, atomic, ionized) according to internal (gas density, pressure, magnetic field) and external (gravitation, radiation field, winds) conditions. Energy is injected into turbulent cascade at the driving length scale (large scale) and dissipated at the dissipation length scale (small scale). We identify the dissipation length scale with the characteristic size of selfgravitating clouds. These clouds decouple from the the turbulent cascade and constitute the first energy sink. The source of energy which is injected at the driving scale to maintain turbulence can be either (i) mass accretion in the gravitational potential of the galactic center (fully gravitational FG model) or (ii) supernova explosions (SN model). In the collisional case energy is also supplied in the process of mass accretion in the gravitational potential of the galactic center and dissipated via partially inelastic cloud–cloud collisions. The actual dissipation rate in individual collisions is largely unknown. The disk evolution is mainly driven by the external mass accretion rate. Since these models are equilibrium models, we assume that the mass accretion rate is constant throughout the region of interest when averaged for a sufficiently long time (∼ Ω−1; here Ω is the angular velocity of circular orbits in the gravitational potential of the galactic nucleus) and maintained for at least the turnover timescale $R/v_{\text{turb}}$ of gas in the disk, where $R$ is the distance from the center of the galaxy and $v_{\text{turb}}$ the characteristic speed of turbulent eddies. All models give access to the global parameters of the disk and local parameters of the most massive clouds (see Table 1). The free parameters of the models are the Toomre parameter $Q$, the disk transparency $\vartheta$ (Eq. 7), and the mass accretion rate $\dot{M}$. Other parameters are fixed using the Galactic values (Vollmer & Beckert 2002, 2003). Each model has an associated star formation rate. In the following we describe these models in more detail.

| Table 1. Model parameters and their meaning |
|-------------------------------------------|
| **large scale** | **disk** |
| $R$ | galactic radius |
| $v_{\text{rot}}$ | rotation velocity |
| $\Omega$ | angular velocity |
| $M_{\text{dyn}}$ | total enclosed (dynamical) mass |
| $M_{\text{gas}}$ | total gas mass |
| $v_{\text{turb}}$ | gas turbulent velocity dispersion |
| $Q$ | Toomre parameter |
| $\varrho$ | midplane density |
| $\Sigma$ | surface density |
| $H$ | disk height |
| $\dot{M}$ | disk mass accretion rate |
| $\nu$ | viscosity |
| $l_{\text{driv}}$ | turbulent driving length scale |
| $\delta$ | scaling parameter between driving scale length and cloud size |
| $\Phi_{V}$ | cloud volume filling factor |
| $\zeta$ | viscosity scaling parameter |
| $H_{\text{ff}}$ | disk vertical free fall time |
| $\dot{n}$ | star formation rate per unit volume |
| $\Sigma_{*}$ | star formation rate per unit surface |
| $M_{*}$ | star formation rate |
| $\xi$ | conversion factor for SN energy flux |
| $\eta$ | star formation efficiency in the collisional model |
| $\gamma$ | linking factor between $M_{\text{gas}}$, $\dot{M}$ for torus evolution |
| $\vartheta$ | disk transparency |
| $M_{\text{BH}}$ | mass accretion rate onto the black hole |
| $M_{\text{wind}}$ | wind outflow rate |
| $J_{\text{UV}}$ | AGN UV radiation field |
| **small scale** | **clouds** |
| $t_{\text{coll}}$ | timescale for cloud – cloud collisions |
| $t_{\text{coll}}$ | cloud mean free path |
| $M_{\text{cl}}$ | cloud mass |
| $v_{\text{cl}}$ | cloud radius |
| $N_{\text{cl}}$ | cloud surface density |
| $c_{\text{s}}$ | local sound speed within the clouds |
| $c_{\text{ff}}$ | sound crossing time of clouds |
| $t_{\text{ff}}$ | cloud free fall time |
| $T$ | temperature |
| $c_{\text{i}}$ | sound crossing time of the ionized gas |
itself. The viscosity is usually assumed to be proportional to the thermal sound speed. Thus, the (gas) heating rate depends itself on the gas temperature. This leads to an equilibrium corresponding to a thermostat mechanism. Instead, we use energy flux conservation, where the potential energy that is gained through mass accretion and differential rotation is cascaded by turbulence from large to small scales and dissipated there.

One fundamental approximation is that the kinetic energy is dissipated (removed from the turbulent cascade) when the gas clouds become self-gravitating. Turbulence transfers the energy from the driving wavelength $l_{\text{driv}}$ to the dissipation wavelength $l_{\text{diss}}$, which corresponds to the size of the largest self-gravitating clouds. The two length scales are linked by the scaling parameter $\zeta$. For a Kolmogorov-like turbulent energy spectrum $\zeta = (l_{\text{driv}}/l_{\text{diss}})^{2}$. In addition, the modeled disks have a constant Toomre-$Q$ parameter:

$$Q = \frac{v_{\text{turb}} \Omega}{\pi G \Sigma} \geq 1,$$  \hspace{1cm} (1)

where $v_{\text{turb}}$ is the turbulent velocity, $\Omega$ the angular velocity, $G$ the gravitational constant, and $\Sigma$ the gas surface density of the disk. If we can approximate the total gas mass within a radius $R$ by $M_{\text{gas}} = \pi R^{2} \Sigma$ the Toomre parameter can be rewritten

$$Q = \frac{v_{\text{turb}}}{v_{\text{rot},K}} \frac{M_{\text{gas}}}{M_{\text{dyn}}},$$  \hspace{1cm} (2)

where $M_{\text{dyn}}$ is the total enclosed mass and $v_{\text{rot}}$ the Keplerian rotation velocity.

Furthermore, we use the following prescription for the viscosity:

$$\nu = \zeta^{-1} v_{\text{turb}} l_{\text{driv}}.$$  \hspace{1cm} (3)

We obtained a set of equations with 3 free parameters: the Toomre parameter $Q$, the scaling parameter $\zeta > 1$, and the mass accretion rate within the disk $\dot{M}$. The mass accretion rate is the gas mass transported per time through the gas disk from large to small radii. It must be supplied from the galaxy at the outer radius of the turbulent gas disk and is constant at all radii in the disk. This set of equations can be solved analytically and the results were already used in Paper I to describe properties of our Galaxy. The solutions depend on the parameters $Q$, $\zeta$, $M$, $v_{\text{rot}}$, and $R$. It turned out that the driving wavelength equals the disk height $l_{\text{driv}} = H$.

In a second step we included the energy input due to supernova (SN) explosions (Vollmer & Beckert 2003, Paper II). The energy flux provided by SNe is transferred by turbulence to smaller scales where it is again dissipated. The SN energy flux is assumed to be proportional to the local star formation rate. The local star formation rate $\dot{\rho}_{s}$ is taken to be proportional to the mean density and inversely proportional to the local free fall time of the clouds. These clouds have sizes that are a factor $\delta$ smaller than the driving length scale. The factor of proportionality is the probability to find a self-gravitating cloud, i.e. the volume filling factor. The integration length in the vertical $z$ direction is assumed to be the turbulent driving scale length, i.e. the vertical height in the disk where self-gravitating clouds are found: $\Sigma_{s} = \dot{\rho}_{s} l_{\text{driv}}$. The SN energy per unit time $\dot{E}_{\text{SN}}$ per area $\Delta A$ is therefore proportional to the local star formation rate $\dot{\Sigma}_{s}$:

$$\frac{\dot{E}_{\text{SN}}}{\Delta A} = \zeta \dot{\Sigma}_{s},$$  \hspace{1cm} (4)

where the factor of proportionality $\zeta$ is independent of the radius in the disk. Its normalization with Galactic values yields $\zeta = 4.6 \times 10^{-8} \text{ (pc/yr)}^{2}$.

In the FG model the energy transported through the turbulent cascade is supplied by mass accretion, which leads to an energy flux equation of the form

$$\rho v_{\text{turb}}^{2} l_{\text{driv}} = \xi \dot{\Sigma}_{s}.$$  \hspace{1cm} (5)

In the case of SN driven turbulence the energy flux is determined by the star formation rate

$$\rho v_{\text{turb}}^{2} l_{\text{driv}} = \xi \dot{\Sigma}_{s}.$$  \hspace{1cm} (6)

Furthermore, we take into account that the clouds are formed during the interaction between SN remnants at the compressed edges. The size of the clouds $l_{cl}$ is consequently smaller than the turbulent driving wavelength and we use $\delta = l_{\text{driv}}/l_{cl}$ with $\delta \geq 1$.

### 2.2. Collisional disks and the stability of the clouds

If the selfgravitating clouds are stable, their collisions will give rise to angular momentum redistribution again described by an effective viscosity. An equilibrium disk can be formed if there are fragmenting collisions or partially elastic collisions (the clouds are supposed to be magnetized). If the collisional timescale $t_{\text{coll}}$ is longer or equal to the dynamical timescale, the resulting viscosity can be written as

$$\nu = \vartheta^{-1} v_{\text{turb}} H,$$  \hspace{1cm} (7)

where the disk transparency $\vartheta = t_{\text{coll}}/\Omega > 1$ and $H$ is the disk height. It follows that the collisional energy dissipation rate is

$$\frac{\Delta E}{\Delta A \Delta t} = f \frac{\Sigma v_{\text{turb}}^{2}}{t_{\text{coll}}} = f \frac{\Sigma l_{\text{diss}}^{2} v_{\text{turb}}^{2}}{t_{\text{coll}}} = f \frac{\Sigma l_{\text{driv}}^{2} v_{\text{turb}}^{2}}{\vartheta H}.$$  \hspace{1cm} (8)

Here the factor $f$, which has been omitted in Vollmer et al. (2004), accounts for the mean fraction of cloud mass participating in the highly supersonic cloud collisions. For constant density clouds Krolik & Begelman (1988) argue that $f = 0.2$. For more centrally condensed, self-gravitating clouds we will use a factor $f = 0.1$ in this paper. This geometric factor $f$ not only reduces the average energy dissipation rate in cloud collisions but also the angular momentum redistribution in the collisions. The reduced energy dissipation is accompanied by a correspondingly reduced mass accretion rate $\dot{M}$ for the same transparency in the model disks $\nu \rightarrow f \nu$ in Eq.(7).

Since in the FG model $l_{\text{driv}} = H$, the FG model and the collisional model are formally equivalent. We can thus use Eq. (5) replacing $\zeta$ by $\vartheta$ to describe the collisional model. Nonetheless the interpretation of $\zeta$ and $\vartheta$ is completely different.
The cloud size \( r_{cl} \) and the volume filling factor \( \Phi_V \) of clouds can be derived using their mean free path (see Vollmer et al. 2004)

\[
l_{\text{coll}} = \vartheta H = \frac{4r_{cl}}{3\Phi_V}
\]

and the fact that the clouds are self-gravitating

\[
t^s_{\text{ff}} = \sqrt{\frac{3\pi\Phi_V}{32G\rho}} = t_s = \frac{r_{cl}}{c_s},
\]

where \( t^s_{\text{ff}} \) is the free fall timescale within clouds, \( \rho \) the density, \( t_s \) the sound crossing timescale, and \( c_s \) the sound speed. This leads to

\[
r_{cl} = \frac{\pi^2}{8} \frac{Qc_s^2}{\Omega v_{\text{turb}} \vartheta}
\]

and

\[
\Phi_V = \frac{\pi^2}{6} \frac{Qc_s^2}{v_{\text{turb}} \vartheta}. \tag{12}
\]

The cloud mass is then

\[
M_{cl} = \frac{4\pi}{3} \Phi_V^{-1} \rho r_{cl}^3 = \frac{2+\pi^4}{64} c_s^4 \vartheta^{-\frac{4}{3}} G^{-\frac{4}{3}} Q^{\frac{4}{3}} f^{\frac{4}{3}} \dot{M}^{-\frac{4}{3}} \Omega^{-1}. \tag{13}
\]

These clouds move supersonically within the intercloud gas. If the intercloud gas is ionized, typical Mach numbers are about 10. Therefore, we expect that the clouds might be destroyed by Rayleigh-Taylor instabilities. However, Rödiger & Hensler (2008) showed that these instabilities are suppressed in the presence of (i) a sufficiently strong gravitational field of the clouds or (ii) a strong magnetic field. The ram pressure exerted on the clouds is \( p_{\text{ram}} = \rho_{int} v_{cl}^2 \), where \( \rho_{int} \) is the intercloud gas density and \( v_{cl} \) is the cloud velocity. Following Rödiger & Hensler (2008) Rayleigh-Taylor instabilities are suppressed if the gravitational acceleration \( g \) is higher than the acceleration due to the drag by ram pressure \( a_D \). This yields approximately:

\[
g \sim \frac{M_{cl}G}{r_{cl}^2} > a_D \sim \frac{p_{\text{ram}}}{\Sigma_{cl}}. \tag{14}
\]

For the intercloud gas density we use the value of the Galactic Center \( \rho_{int} = 10^3 \text{ cm}^{-3} \) (Erickson et al. 1994). Using \( M_{cl} = 10^5 M_\odot \), \( r_{cl} = 0.02 \text{ pc} \), \( v_{cl} = 100 \text{ km s}^{-1} \), the gravitational acceleration is about 4 times higher than the ram pressure drag. If the intercloud gas has a 10 times higher density, only a magnetic field with a field strength of \( B \sim \sqrt{10} \rho_{int} v_{cl}^2 \sim 1 \text{ mG} \) can stabilize the clouds. This kind of field strength is observed in the Circumnuclear Disk in the Galactic Center (Plante et al. 1995). It is thus plausible that the torus clouds are stable against Rayleigh-Taylor instabilities.

3. Star formation in clumpy gas disks

3.1. Turbulent disks

Following Paper II we assume that the star formation rate is proportional to the mean density of the disk and the inverse of the characteristic timescale for the cloud collapse, i.e. the non-averaged local free fall time \( t^s_{\text{ff}} \):

\[
\dot{\rho}_* \propto \frac{\rho}{t^s_{\text{ff}}}. \tag{15}
\]

Since \( t^s_{\text{ff}} \propto \rho^{-\frac{2}{3}} \) this corresponds to a Schmidt law of the form \( \dot{\rho}_* \propto \rho^\eta \). The factor of proportionality is given by the probability to find a self-gravitating cloud, i.e. the volume filling factor \( \phi_V \). Thus, the star formation rate is given by

\[
\dot{\rho}_* = \phi_V \rho \rho \left( \frac{t^s_{\text{ff}}}{t^s_{\text{ff}}}, \right) = \sqrt{\phi_V \rho \rho \left( \frac{t^s_{\text{ff}}}{t^s_{\text{ff}}}, \right)}.
\]

Furthermore, we assume that stars are only born in the mid-plane of the disk in regions that have the size of the turbulent driving length scale \( l_{\text{driv}} \), because the clouds can collapse only within the turbulent timescale \( t_{\text{turb}} = l_{\text{driv}}/v_{\text{turb}} \). We thus obtain

\[
\dot{\Sigma}_* = \dot{\rho}_* l_{\text{driv}} \tag{17}
\]

for the mass surface density turned into stars.

3.2. Collisional disks

For the collisional disk we assume that the star formation rate is proportional to the overall density \( \rho \) and the cloud collision frequency \( t^{-1}_{\text{coll}} = \vartheta^{-1} \Omega \):

\[
\dot{\rho}_* = \eta \rho \vartheta^{-1} \Omega, \tag{18}
\]

where \( \eta \) is an a priori unknown efficiency factor. In terms of stellar mass per time this gives

\[
\dot{M}_* = \eta M_{\text{gas}} \vartheta^{-1} \Omega. \tag{19}
\]

4. Thick disks in a generic galactic center

The theoretical model described in the previous sections can now be applied to recent near-IR high-spatial resolution SINFONI observations of nearby AGN. Davies et al. (2007) showed that there had been recent star formation in the central few tens of parsecs in a sample of nearby AGN. Following on from this, Hicks et al. (2008) showed that distribution and kinematics of the central concentrations of gas were similar to those of the stars, and was geometrically thick with \( v_{\text{turb}}/v_{\text{rot}} > 1/2 \). They argued that this gas comprised the large scale structure of the tori, implying that tori can form stars. And they gave an estimate for the gas mass in this region as 10% of the dynamical mass. Before we derive the physical disk parameters for the individual AGNs observed by Davies et al. (2007), we give an overview over the different types of thick tori. Note that \( \vartheta \) is the disk transparency, i.e. \( \vartheta \leq 1 \) implies an opaque disk whereas a large \( \vartheta \) results in a transparent disk. For a generic galactic center we assume a dynamical mass (which for radii \( R \) larger than a few pc is dominated by the stellar content), of \( M_{\text{dyn}} = 10^8 M_\odot \) and a gas mass of \( M_{\text{gas}} = 10^7 M_\odot \), both within a radius of \( R = 20 \text{ pc} \). The enclosed mass leads to a rotation velocity of 150 km s\(^{-1}\) at this radius. In addition, we adopt a cloud internal sound speed of
ce = 1.5 km s\(^{-1}\). The value for the sound speed corresponds to a cloud temperature of \(\sim 500\) K when only thermal gas pressure is considered. The sound speed is a measure of the pressure support against self-gravity and additional contributions to the pressure gradient inside clouds like magnetic fields may contribute. The adopted sound speed leads to cloud masses of \(M_{\text{cl}} \propto c^4_e \sim 10 M_\odot\). The disk is stable with a Toomre parameter of \(Q = 4.7\) for a turbulent velocity supporting the vertical thickness of \(v_{\text{turb}} = 70\) km/s. Moreover, we assume a star formation rate of \(\dot{M} = 0.1 M_\odot\text{yr}^{-1}\). This can be considered an upper limit to the current star formation rate in the central few tens of parsecs. Davies et al. (2007) showed that while star formation had occurred there recently, it has now ceased. Based on the exponentially decaying starburst model they used and the time averaged star formation rates they estimated, the current rates are expected to be below this limit.

In the following we generate a generic set of models which (i) can describe different evolutionary phases of a \(\sim 20\) pc scale gas disk in terms of mass accretion rate, disk thickness/transparency, and star formation rate and (ii) can reproduce the observations at a generic time in the evolutionary sequence. We first compare different disk models, representing evolutionary stages, to the observations of the current state of the disk (Sec. 4.1–4.5). It is shown that a massive accretion event leads to a relatively thin turbulent disk which forms stars at a high rate (SN model). Once the SN explode the intercloud medium is blown out, leaving only dense, compact clouds. This results in a collisional disk that may assume one of several states (Sec. 4.2–4.5) depending on the external mass accretion rate \(\dot{M}\), the Toomre \(Q\), and transparency \(\vartheta\) parameters. In Sec. 5 we then investigate the evolution of the collisional disk.

### 4.1. A massive turbulent disk creates a starburst

We first try applying the turbulent SN disk model. With the parameters described above it would have a mass accretion rate

\[
\dot{M} = 2.18 \dot{M}_*^{-1} M_{\text{gas}}^2 v_{\text{turb}}^4 R^{-2} \xi^{-1}
\]

in excess of \(10^9 M_\odot\text{yr}^{-1}\) and a ratio between the turbulent driving and dissipation length scales of

\[
\delta = 1.17 \dot{M}_*^{-3} G^3 M_{\text{gas}}^6 v_{\text{turb}}^2 R^{-6} \xi^{-2} > 10^4.
\]

Such a model can be discarded, because its mass accretion rate is far too high with respect to any supply from the outer galaxy and the lifetime \(M_{\text{gas}}/\dot{M} = 10^4\) yr is shorter than the dynamical time \(\Omega^{-1} \sim 10^5\) yr.

On the other hand, if we assume that a turbulent SN disk is responsible for the starburst with a star formation rate of \(\dot{M}_* = 1 M_\odot\text{yr}^{-1}\) (comparable to the initial rate inferred by Davies et al. 2007) and that the turbulent velocity was lower \((v_{\text{turb}} = 20\) km s\(^{-1}\)) than the present collisional disk, we find a mass accretion rate of \(\dot{M} = 2 M_\odot\text{yr}^{-1}\) and \(\delta = 23\). These values are close to the values for the large-scale Galactic disk (see Paper II). A typical cloud has a radius of \(r_{\text{cl}} = 0.1\) pc and a mass of \(M_{\text{cl}} = 10^5 M_\odot\). This kind of disk contains about a thousand clouds within \(R = 20\) pc.

We conclude that a viable collisional massive gas disk has a rather low turbulent velocity and is therefore moderately thin with \(H/R = v_{\text{turb}}/v_{\text{rot}} \sim 0.13\). It then yields large star formation rates of the order of one solar mass per year. This represents a starburst which subsequently will destroy the disk once the supernovae explode after about 10 Myr. These explosions do not cause any harm to the densest and most massive clouds, but they clear the space between the clouds, i.e. they remove the initial intercloud medium. We are then left with a collisional disk.

### 4.2. A massive, opaque, collisional disk

\((Q = 5, \vartheta = 1)\)

The collisional disks can be distinguished by their \(Q\) and \(\vartheta\) parameters. We start with collisional and opaque disks, i.e. the mean free path of the clouds is about the height of the disk \(H\). This implies that along a vertical path through the disk there is on average one intervening cloud. Along a path in the disk midplane towards the center there are typically \(N \sim 10\) clouds blocking the direct view. Collisions are frequent in such a torus or disk. This yields a mass accretion rate of

\[
\dot{M} = 2 \frac{v_{\text{turb}}^3}{GQ\vartheta} = 3.4 M_\odot\text{yr}^{-1}.
\]

The volume filling factor of the clouds is \(\Phi_{V} = 0.004\), the clouds have typical radii of \(r_{\text{cl}} = 0.02\) pc, and masses of \(M_{\text{cl}} = 15 M_\odot\).

### 4.3. A massive, transparent, collisional disk

\((Q = 5, \vartheta = 10)\)

The large mass accretion rate in the above model (Sec. 4.2) depends linearly on the collision rate and is a consequence of the low transparency. If the disk is more transparent, \(\vartheta = 10\), the mass accretion rate is therefore \(\dot{M} = 0.3 M_\odot\text{yr}^{-1}\), the volume filling factor of the clouds is \(\Phi_{V} = 4 \times 10^{-5}\), and the clouds have typical radii of \(r_{\text{cl}} = 0.002\) pc and masses of \(M_{\text{cl}} = 1.5 M_\odot\). We see that for the same Toomre-\(Q\) a larger transparency implies smaller and less massive clouds with smaller volume filling factors.

### 4.4. A light, opaque, collisional disk

\((Q = 50, \vartheta = 1)\)

If clouds are large and less dense we can have a disk which is light but still optically opaque due to dust in the clouds. For this disk class we assume a gas mass of only 1% of the dynamical mass, i.e. \(M_{\text{gas}} = 10^6 M_\odot\). This yields a mass accretion rate of \(\dot{M} = 0.3 M_\odot\text{yr}^{-1}\). The volume filling factor is \(\Phi_{V} = 0.04\), and the typical cloud radii and masses are \(r_{\text{cl}} = 0.2\) pc and \(M_{\text{cl}} = 150 M_\odot\).

### 4.5. A light, transparent, collisional disk

\((Q = 50, \vartheta = 10)\)

The last disk class is transparent, \(\vartheta = 10\), and has a small gas mass, \(M_{\text{gas}} = 10^6 M_\odot\). It has the lowest mass accretion rate, \(\dot{M} = 0.03 M_\odot\text{yr}^{-1}\), and a low volume filling factor, \(\Phi_{V} = \ldots\)
4 \times 10^{-4}. The collisional disks described above can be identified with the observed high mass accretion leads to a massive, opaque disk and (ii) a \((Q = 5, \vartheta = 1)\)-disk and a \((Q = 50, \vartheta = 10)\)-disk share clouds of the same mass and size. These clouds are very similar to those found in the Galactic Center (see Vollmer et al. 2004). We thus can draw up a disk evolution in which a massive, opaque disk evolves with time into a light, transparent disk.

For the rest of the article we assume that the cloud mass of all disks is \(M_{\text{cl}} = 10^{3} \, M_{\odot}\). This is equivalent to a common column density of all clouds of \(N_{\text{cl}} \sim 10^{24} \, \text{cm}^{-2}\).

5. Torus evolution

The collisional disks described above can be identified with the observed 30 pc-scale gas concentrations observed by Davies et al. (2007) and Hicks et al. (2008) which arguably correspond to the large scale structure of AGN tori.

It is now investigated how a collisional torus can evolve from a massive to a less massive state. To do so we assume that the gas mass of the torus is proportional to its mass accretion rate

\[ M_{\text{gas}} = 2^{-\frac{3}{4}} G^{-\frac{4}{3}} \vartheta^{\frac{1}{3}} Q^{-\frac{4}{3}} f^{-\frac{2}{3}} \dot{M}^{\frac{4}{3}} v_{\text{rot}} R = \gamma \dot{M}^{x} . \]  
(24)

In this way we subsume all possible time dependencies of various parameters and their correlations in the time evolution of \(\dot{M}\). Together with Eq. 13 this yields

\[ \vartheta = \frac{\pi^{4} c_{s}^{2} R^{4}}{64 \gamma M_{\text{cl}} G^{2} M^{x}} . \]  
(25)

The expressions for the Toomre parameter, the turbulent velocity, and the star formation rate are then

\[ Q = \frac{\pi^{2} c_{s}^{2} R^{4} \Omega^{\frac{1}{2}}}{\sqrt{128} \gamma^{2} G^{2} M_{\text{cl}} f^{\frac{1}{2}} M^{2 x^{-\frac{1}{2}}}} , \]  
(26)

\[ v_{\text{turb}} = \frac{\pi^{2} c_{s}^{2} R^{2} \Omega^{\frac{1}{2}}}{\sqrt{128} \gamma M_{\text{cl}} G f^{\frac{1}{2}} M^{2 x^{-\frac{1}{2}}}} , \]  
(27)

and

\[ \dot{M}_{*} = \frac{\eta}{\pi^{4}} \frac{64 M_{\text{cl}} c_{s}^{2} G^{2} \Omega}{c_{s}^{2} R^{2}} M^{2 x} . \]  
(28)

In this way the behavior of the transparency, Toomre parameter, thickness of the disk via \(H = v_{\text{turb}}/\Omega\), and star formation rate can be identified with the change of the external mass accretion rate. For our stationary equilibrium disks to be applicable we must require the change of the external mass accretion to be slow, so that the whole disk can adjust to the changing external conditions. This time for adjustment \(t_{\text{eq}}\) is approximately the ratio between the torus gas mass and mass accretion rate. For typical values of \(M_{\text{gas}} \sim 10^{7} \, M_{\odot}\) (Tab. 2) and \(\dot{M} \sim 1 \, M_{\odot} \, \text{yr}^{-1}\) (Tab. 3) this leads to \(t_{\text{eq}} \sim 10\) Myr. This is smaller than the observed starburst ages (Tab. 2) for all AGNs except NGC 1097 where the time of adjustment and the starburst age are comparable.

5.1. Evolution at constant thickness

Whenever the disk thickness stays the same during its evolution, \(v_{\text{turb}} = \text{const.} \, \text{in time}, \) and subsequently \(x = \frac{1}{2}\) (Eq. 27), this implies that the external mass accretion rate stays at a high level. The gas mass, star formation rate, \(\vartheta\), and the Toomre Q parameter depend on the mass accretion rate \(\dot{M}\) in the following way:

\[ M_{\text{gas}} \propto \dot{M}^{\frac{2}{3}} , \quad M_{*} \propto \dot{M} , \quad \vartheta \propto \dot{M}^{-\frac{1}{3}} , \quad Q \propto \dot{M}^{-\frac{2}{3}} . \]  
(29)

The dependence of these parameters on the gas mass is then:

\[ M_{\text{gas}} \propto M^{\frac{2}{3}} , \quad \vartheta \propto M_{\text{gas}}^{-1} , \quad Q \propto M_{\text{gas}}^{-1} \]  
(30)

and the relation for the cloud mass and the volume filling factor are:

\[ M_{\text{cl}} = \text{const.} , \quad \Phi_{V} \propto M_{\text{gas}} . \]  
(31)

It is remarkable that the star formation rate is linearly coupled to the mass accretion rate in this scenario.

5.2. Evolution at constant mass

Alternatively, at later stages when the mass accretion rate is low and changes little, the torus mass may stay constant, \(M_{\text{gas}} = \text{const.} , \) and subsequently \(x = 0\) (Eq. 27). The turbulent velocity dispersion, star formation rate, \(\vartheta\), and the Toomre Q depend on the mass accretion rate \(\dot{M}\) now in the following way:

\[ v_{\text{turb}} \propto \dot{M}^{\frac{1}{2}} , \quad \dot{M}_{*} = \text{const.} , \quad \vartheta = \text{const.} , \quad Q \propto \dot{M}^{\frac{1}{2}} . \]  
(32)

The relation for the cloud mass and the volume filling factor are:

\[ M_{\text{cl}} = \text{const.} , \quad \Phi_{V} \propto \dot{M}^{-\frac{1}{2}} . \]  
(33)

At constant disk mass and decreasing external mass supply the disk will become geometrically thin without changing the transparency.

An interesting result is that during both types of torus evolution—at constant turbulent velocity and at constant gas mass—the cloud mass does not change.

6. Torus evolution scenarios

In the picture of quasi-stationary equilibrium disks driven by cloud collisions the evolution will be determined by the external mass accretion rate, i.e. the mass inflow from distances > 100 pc. We divide the torus evolution into three phases:

- **Phase I: Initial massive infall and formation of a turbulent, massive gas disk:**
  An initial rapid infall of a large amount of gas, \(M_{\text{gas}} \sim\)
10^7 \ M_\odot, within a short time (\(\Delta t < 1 \ \text{Myr}\); \(\dot{M} > 10 \ \dot{M}_\odot\ \text{yr}^{-1}\)) leads to the formation of a massive (\(Q \sim 1\), moderately thin (\(v_{\text{turb}}/v_{\text{rot}} < 5\)) gas disk in which star formation proceeds. This phase will be recognized as a starburst. The disk becomes turbulent and the turbulence is maintained by the energy input from stellar winds. After \(\sim 10 \ \text{Myr}\) the first SN explode and will rapidly remove the initial intercloud medium from the disk. Only the most massive and densest clouds which are not Jeans unstable will survive. This leads in the following to a collisional torus.

- **Phase II:** Torus evolution at constant turbulent velocity:
  During the first phase of its evolution the massive collisional torus stays thick. This implies that the mass accretion rate within the torus, and thus also the external mass accretion rate \(\dot{M}\), do not decrease significantly during this phase. The gas mass and the cloud collision rate (\(t_{\text{coll}} \propto \vartheta^{-1}\)) decrease with decreasing \(\dot{M}\), whereas \(Q\) increases with the square root of the external mass accretion rate. The star formation rate within the torus decreases with decreasing \(\dot{M}\) (Eq. 30).

- **Phase III:** Torus evolution at constant gas mass:
  Once the external mass accretion rate has significantly decreased, the torus evolves at constant gas mass. The velocity dispersion and \(Q\) decrease with the square root of the external mass accretion rate, whereas the cloud collision rate (\(t_{\text{coll}} \propto \vartheta^{-1}\)) and the star formation rate stays constant (Eq. 32). The Circumnuclear Disk (CND) in the Galactic Center (Güsten et al. 1987) represents such a late stage (\(Q = 190\), \(\vartheta = 15\); Vollmer et al. 2004) of the torus to disk evolution.

Depending on the time evolution of the external mass accretion rate (from distances larger than 100 pc) we suggest three possible evolution scenarios (Fig. 1):

- **Scenario I:**
  The torus never reaches Phase I, because (i) it is already clumpy from the very beginning, (ii) there is already star formation occurring at scales of \(\sim 10\) pc from the galactic center; the associated SN explosions and/or winds remove the existing intercloud medium and/or inhibit the formation of an intercloud medium. The two possibilities imply that the initial mass accretion rate is not very high. A third possibility (iii) is that the disk’s velocity dispersion is prohibitively large to allow a \(Q = 1\) disk. In this case star formation proceeds via cloud-cloud collisions. The star formation rate is lower than that of a massive turbulent disk. The rate of momentum injection due to SNe and stellar winds is
  \[
  F = p_s \Delta A = 5 \times 10^{33} \left( \frac{\dot{M}_*}{\dot{M}_\odot \text{yr}^{-1}} \right) \text{dyne},
  \]
  where \(p_s\) is the pressure due to SNe and stellar winds exerted on a surface \(\Delta A\) (Veilleux et al. 2005). Assuming the same initial turbulent velocity for the clouds and the intercloud medium, the intercloud medium can be removed from the disk if \(p_s \geq \rho_{\text{IM}} \Phi_{\text{V}}^{\text{IM}} v_{\text{turb}}\), where \(\rho_{\text{IM}}\) and \(\Phi_{\text{V}}^{\text{IM}}\) are the density and the volume filling factor of the intercloud medium. Assuming \(\dot{M}_* = 0.02 \ \dot{M}_\odot\ \text{yr}^{-1}\), \(R = 10\) pc (Sect. 6), and \(v_{\text{turb}} = 50 \ \text{km s}^{-1}\) (Tab. 2) leads to \(n_{\text{IM}} \Phi_{\text{V}}^{\text{IM}} \leq 10^3 \ \text{cm}^{-3}\). Since the disk volume averaged density of the clouds is \(n_{\text{IM}} \Phi_{\text{V}} = 10^4 \ \text{cm}^{-3}\) (Tab. 4), the intercloud space can only be cleared by SN explosions and stellar winds if the intercloud medium contains less than \(\sim 10\%\) of the total disk mass.

- **Scenario II:**
  Due to an initial, massive infall a massive (\(Q \sim 1\)) turbulent star-forming disk is formed (Phase I). The turbulence in this disk is maintained through the energy supply by feedback from rapid star formation. The subsequent SN explosions destroy the disk structure after 10 Myr, i.e. the intercloud medium is removed leaving only the densest, most massive clouds which remain Jeans-stable. The disk becomes collisional and stays geometrically thick (Phase II). After \(\sim 100\) Myr the mass accretion rate decreases and the disk becomes thin (Phase III) and ultimately transparent (\(\vartheta > 5\)). The time at which the torus changes from Phase II into Phase III depends on the time evolution of the external mass accretion rate in this scenario.

- **Scenario III:**
  Due to an initial massive infall event, a massive (\(Q \sim 1\)) turbulent star-forming disk appears (Phase I). As in Scenario II, SN explosions destroy the disk structure after \(\sim 10\) Myr, the intercloud medium is removed and only the densest, most massive clouds are left over, which are Jeans-stable. The disk becomes collisional and will stay thick as long as the external mass accretion rate is sufficiently high (Phase II). Due to a secondary massive and rapid gas infall a second massive (\(Q \sim 1\)) turbulent star-forming disk can form (Phase I), which evolves again into a collisional disk after \(\sim 10\) Myr (Phase II). After \(\sim 100\) Myr the mass accretion rate has sufficiently decreased and the disk becomes thin (Phase III) and ultimately transparent (\(\vartheta > 5\)). The time at which the torus changes from Phase II into Phase III depends again on the time evolution of the external mass accretion rate.

7. Applying the observations

The scenarios of Sect. 6 derived from our analytical models can now be compared with the VLT SINFONI observations of Davies et al. (2007) and Hicks et al. (2008). As has been shown in Sect. 4, the present state of the disk can only be described consistently by a collisional disk model. The comparison with observations will allow us to derive the parameters of (i) the present torus, (ii) the initial torus immediately after Phase I, (iii) the massive (\(Q \sim 1\)) turbulent gas disk that gave rise to the initial starburst (scenario II and III), and (iii) the star formation efficiency of the collisional phase.

The observables, i.e. the input parameters for our analytical model, are the radius from the galactic center \(R\), the rotation velocity \(v_{\text{rot}}\), the turbulent velocity dispersion \(v_{\text{turb}}\), the gas mass \(\dot{M}_{\text{gas}}\), the peak star formation rate during the initial starburst \(\dot{M}_{\text{peak}}\), and the age of the initial starburst \(t_{\text{SB}}\). We assume for all AGN, except NGC 1097, a starburst duration of 10 Myr,
The dispersion type and the radius within which the subsequent parameters found in Table 2. For each object, the table gives its Seyfert sufficiently well known. The parameters for these objects can be Davies et al. (2007) for which these input parameters are suf-ficient only apply our model to a subsample of 6 nearby AGNs from i.e. the starburst continues until the first SN explode. We only apply our model to a subsample of 6 nearby AGNs from Davies et al. (2007) for which these input parameters are sufficiently well known. The parameters for these objects can be found in Table 2. For each object, the table gives its Seyfert type and the radius within which the subsequent parameters apply. The dispersion $v_{\text{turb}}$ is the value measured from the data (after accounting for instrumental broadening), while the rotation velocity $v_{\text{rot}}$ is a Keplerian equivalent value. This means that it represents the rotation velocity that would be needed if ordered circular motions in a single plane supported the entire dynamical mass. It is therefore significantly greater than the measured rotation speed. The gas mass $M_{\text{gas}}$ is difficult to derive. Hicks et al. (2008) estimated it from a combination of diagnostics, including the 1.3 mm CO luminosity, the 2.12 $\mu$m H$_2$-1-0(S(1)) luminosity, and a comparison to the gas-to-dynamical mass ratios in other spiral and starburst galaxies. The peak star formation rates $M_{\text{gas}}^{\text{peak}}$ are derived from the starburst models used in Davies et al. (2007). They are simply the star formation rates required to form the young stars in a timescale of 10 Myr (in contrast to the time-averaged rates given in that paper). The only exception is NGC 3783, for which we have adopted a 2-starburst model with ages of 110 Myr and 30 Myr. Such models were not considered by Davies et al. (2007) because of the limited number of diagnostics. In our scenario with stronger theoretical constraints on the models we need these additional degrees of freedom to reproduce the observations. The final column gives the age $t_{\text{SB}}$ of the most recent starburst. All equations to derive the properties of the present collisional torus, the massive $(Q \sim 1)$ turbulent gas disk, and the initial collisional torus are given in Table 3.

### 7.1. The present collisional torus

We recall the assumption that all gas clouds have a constant mass of $M_1 = 10 M_{\odot}$. Moreover the sound speed within the clouds is set to $c_s = 1.5$ km s$^{-1}$. The Toomre $Q$ parameter of the present disks is directly calculated from Eq. [1]. We then use the following expressions for $\vartheta$ and the mass accretion rate $\dot{M}$ which follow from the expression derived for the turbulent velocity dispersion in Paper I $v_{\text{turb}} = (GQf^{-1}M)^{\frac{1}{2}}$ and Eq. [13]

\begin{equation}
\vartheta = \frac{\pi^4}{64} G^{-1} Q^{-1} \left( \frac{M_{\text{gas}}}{M_{\text{cl}}} \right)^2 v_{\text{rot}}^{-1} \Omega_{cl}^{-1} \, v_{\text{turb}}^{-1}, \tag{35}
\end{equation}

and

\begin{equation}
\dot{M} = 2 f v_{\text{turb}}^3 G^{-1} Q^{-1} \vartheta^{-1}. \tag{36}
\end{equation}

### Table 3. Equations to derive the disk/torus properties from observations. Velocities are in units of km s$^{-1}$, radii in pc, masses in $M_{\odot}$, and star formation rates in $M_{\odot}$ yr$^{-1}$.

| property | expression |
|----------|------------|
| present collisional torus | $Q_{\text{pr}} = (v_{\text{turb}}/v_{\text{rot}}) (M_{\text{dyn}}/M_{\text{gas}})$ |
| | $\vartheta_{\text{pr}} = 1.9 \times 10^{-9} Q_{\text{pr}} R / (v_{\text{rot}} v_{\text{turb}}^2 M_{\text{cl}})$ |
| | $\dot{M}_{\text{pr}} = 2 (v_{\text{turb}}^3) / (G Q_{\text{pr}} \vartheta_{\text{pr}})$ |
| massive turbulent gas disk | $Q_{\text{disk}} = 9674 M_{\odot}^{\frac{2}{3}} v_{\text{rot}}$ |
| | $M_{\text{gas}}^{\text{disk}} = 3.97 \times 10^5 M_{\odot}^{\frac{2}{3}} R$ |
| | $v_{\text{disk}} = 18.2 M_{\odot}^{\frac{2}{3}}$ |
| initial collisional torus | $\dot{M}_{\text{init}} = M (M_{\text{disk}}^{\text{pr}} / M_{\text{gas}}) ^2$ |
| | $Q_{\text{init}} = Q_{\text{pr}} M_{\text{gas}}^{\text{pr}} / M_{\text{disk}}^{\text{pr}}$ |
| | $\vartheta_{\text{init}} = \vartheta_{\text{pr}} M_{\text{gas}}^{\text{pr}} / M_{\text{disk}}^{\text{pr}}$ |
Table 2. Input parameters from Davies et al. (2007) and Hicks et al. (2008); see Sect. 7 for details

| name          | type | $R$ (pc) | $v_{rot}$ (km s$^{-1}$) | $v_{turb}$ (km s$^{-1}$) | $M_{gas}$ ($10^6$ M$_\odot$) | $M_{peak}$ ($10^6$ M$_\odot$) | $t_{SB}$ (Myr) |
|---------------|------|----------|------------------------|------------------------|-------------------------------|-------------------------------|---------------|
| Circinus      | Sy 2 | 10       | 93                     | 56                     | 2                             | 0.02                          | 80            |
| NGC 3783      | Sy1  | 30       | 88                     | 35                     | 5                             | 0.3                           | 30            |
| NGC 3227      | Sy1  | 30       | 173                    | 95                     | 20                            | 5.0                           | 40            |
| NGC 1068      | Sy2  | 30       | 184                    | 88                     | 20                            | 14.0                          | 200           |
| NGC 1097      | Sy1  | 30       | 122                    | 59                     | 10                            | 1.0                           | 8             |
| NGC 7469      | Sy1  | 30       | 123                    | 63                     | 10                            | 3.0                           | 110           |

Table 4. Parameters of the present collisional tori.

| name          | $M$ ($M_\odot$ yr$^{-1}$) | $Q$ | $\vartheta$ | $\Phi_V$ | $\rho_{cl}$ | $v_{cl}$ (pc) |
|---------------|---------------------------|-----|-------------|----------|-------------|---------------|
| Circinus      | 0.75                      | 5.7 | 1.9        | 1.2      | 3.9         | 0.01          |
| NGC 3783      | 0.07                      | 4.1 | 6.8        | 0.2      | 2.7         | 0.01          |
| NGC 3227      | 4.27                      | 5.5 | 1.7        | 0.5      | 3.9         | 0.01          |
| NGC 1068      | 3.45                      | 5.4 | 1.7        | 1.2      | 1.8         | 0.02          |
| NGC 1097      | 0.59                      | 4.8 | 3.4        | 0.4      | 2.6         | 0.02          |
| NGC 7469      | 0.66                      | 5.1 | 3.4        | 0.6      | 1.8         | 0.02          |

The torus mass accretion rates (Table 4) include the geometric $f = 0.1$ factor introduced in Sec. 2.2. The resulting rates are still higher than the black hole mass accretion rates and the wind mass loss rates discussed in Sec. 3. The parameters derived in this way for our sample of 6 AGNs are shown in Table 2.

All tori show Toomre $Q$ parameters between 4 and 6, i.e. they are massive thick tori. Moreover, 3 AGNs (Circinus, NGC 3227, and NGC 1068) have opaque tori ($\vartheta < 2$), 2 AGNs (NGC 1097 and NGC 7469) show moderately transparent tori ($\vartheta~3~4$), and 1 AGN (NGC 3783) has a transparent torus ($\vartheta > 5$). It is worth noting that two out of the 3 AGNs with opaque tori are classified as Sy2. We find the smallest mass accretion rate for NGC 3783. The highest mass accretion rates (NGC 3227 and NGC 1068) are several ten times higher than that of NGC 3783.

7.2. The massive ($Q \sim 1$) turbulent gas disk

We now derive the parameters of the initial massive turbulent gas disk which gave rise to the initial starburst. For this we apply the SN model (see Sect. 2) where the energy source for maintaining turbulence in the disk is stellar winds. Their energy input is comparable to that of SN explosions (MacLow & Klessen 2004). Therefore we do not need to change the formalism of the SN model. We further assume that the mass accretion rate equals the peak star formation rate given by Davies et al. (2007) (Table 2) and $\delta = 5$, which is the Galactic value (Vollmer & Beckert 2003).

We assume that for all AGNs, except for Circinus and NGC 3783, scenario II is valid. For Circinus we argue below that scenario I applies, because its peak star formation rate is a factor of more than 10 lower when compared to the other starbursts. This does not imply that star formation is not occurring, just that there was no initial massive accretion event. For NGC 3783 scenario III is more applicable, because a single starburst leads to an enormously high initial mass accretion rate compared to the present value, which we think is implausible. The double starburst we have adopted for NGC 3783, which is consistent with the observations of Davies et al. (2007), requires a first intense burst with $M_* = 4.7 M_\odot$ yr$^{-1}$ to have occurred 110 Myr ago, followed by a second distinct burst with $M_* = 0.3 M_\odot$ yr$^{-1}$ only 30 Myr ago.

The Toomre $Q$ parameter, the total gas mass, and the turbulent velocity dispersion can then be calculated using the following expressions:

$$Q = 0.81 G^{-5/2} M_*^{-2/3} \delta^{-2/3} \xi^{-4/3} \frac{v_{rot}}{v_{turb}},$$

$$M_{gas} = 8.5 \times 10^{-5} G^{-5/2} M_*^{-2/3} \delta^{-2/3} \xi^{-1/3} R,$$

$$v_{turb} = 0.82 G^{3/4} M_*^{1/4} \delta^{-1/4} \xi^{-1/4},$$

where $\xi = 4.6 \times 10^{-8}$ (pc/yr)$^2$ (Vollmer & Beckert 2003).

Using a peak star formation rate of $M_* = 0.02 M_\odot$ yr$^{-1}$ for Circinus leads to a gas mass of the massive turbulent disk which is smaller than that of the present collisional torus. We therefore conclude that scenario II (Fig. 1) does not apply to this AGN. Instead, scenario I yields more appropriate results. The nuclear disk in Circinus did not experience a turbulent, supernovae and stellar wind driven $Q \sim 1$ disk.

The gas masses of the turbulent starburst disks is between 10% and 100% higher than the gas mass of the corresponding present collisional torus, except for Circinus. In the course of torus evolution (Fig. 1) the loss of gas mass in the disk is moderate (up to a factor of 2; Tab. 2 and 5). The star forming disks are moderately thin ($v_{rot}/v_{turb} \sim R/H \sim 5-7$) and their Toomre $Q$ parameter is close to unity.

7.3. The initial collisional torus

Since all observed tori are thick (Table 2), they are all in Phase II of their evolution (see Sect. 6), i.e. they evolve at constant thickness or velocity dispersion. This implies the following relation between the gas mass and the mass accretion rate:

$$\dot{M} \propto M_{gas}^2.$$
Table 5. Parameters of the initial massive \((Q \sim 1)\) turbulent gas disk that gave rise to the initial starburst.

| name      | \(M_{\text{gas}}\) \(10^6\) M\(_\odot\) | \(\dot{M}\) \(\text{(M}_\odot\text{yr}^{-1})\) | \(\vartheta_{\text{turb}}\) \(\text{(km}\text{s}^{-1})\) | \(Q\) |
|-----------|--------------------------------|----------------|----------------|-----|
| Circinus  | 0.7                           | 0.02           | 6              | 1.9 |
| NGC 3783 | 6.9                           | 0.3            | 13             | 1.1 |
| NGC 3227 | 24.8                          | 5.0            | 28             | 1.3 |
| NGC 1068 | 40.0                          | 14.0           | 37             | 1.2 |
| NGC 1097 | 11.9                          | 1.0            | 18             | 1.2 |
| NGC 7469 | 19.6                          | 3.0            | 25             | 1.0 |

Table 6. Parameters of the initial collisional tori.

| name      | \(\dot{M}\) \(\text{(M}_\odot\text{yr}^{-1})\) | \(Q\) | \(\vartheta\) |
|-----------|--------------------------------|-----|-------------|
| Circinus  | 2.1                           | 3.4 | 1.1        |
| NGC 3783 | 0.1                           | 3.0 | 5.0        |
| NGC 3227 | 6.5                           | 4.4 | 1.4        |
| NGC 1068 | 13.5                          | 2.7 | 0.9        |
| NGC 1097 | 0.8                           | 4.0 | 2.9        |
| NGC 7469 | 2.6                           | 2.6 | 1.7        |

We can safely assume that the gas mass of the initial collisional torus at the end of Phase I is close to the gas mass of the massive \((Q \sim 1)\) turbulent disk (Table 5). For Circinus we estimate the gas mass of the initial collisional torus by postulating that the disk was initially opaque, i.e. \(\vartheta \sim 1\). This leads to an initial gas mass of \(M_{\text{gas}} = 3.4 \times 10^6\) M\(_\odot\) at the beginning of Phase II.

For all other AGN a continuous transition from phase I to II provides the mass accretion rate of the initial collisional torus. The \(Q\) and \(\vartheta\) parameters can then be calculated using the following expressions (see Sect. 5):

\[
Q \propto M_{\text{gas}}^{-1}, \quad \vartheta \propto M_{\text{gas}}^{-1}.
\]

Four of the initial collisional disks at the beginning of Phase II (Circinus, NGC 3227, NGC 1068, and NGC 7469) had Toomre \(Q\) parameters around \(Q = 3\) and \(\vartheta\) close to unity, i.e. they were massive and opaque. Two initial collisional disks (NGC 3783 and NGC 1097) had been massive and transparent.

7.4. The evolution of the torus mass accretion rate

In this section we investigate the evolution of the torus mass accretion rate with time in Phase II (see Sect. 6). For this we plot in Fig. 2 the fraction between the mass accretion rate of the present collisional torus and that of the initial collisional torus (end of Phase I and beginning of Phase II) as a function of time for our sample. To determine the time that a given torus passed in Phase II, we place ourselves in scenario II (Fig. 1) and adopt the starburst ages of Davies et al. (2007) for all AGNs except NGC 3783. We assume scenario III for this galaxy, i.e. the occurrence of two distinct starbursts. This leads to an estimated age of the most recent starburst of 30 Myr. The solid line is meant to guide the eye. Based on this plot we conclude that the mass accretion rate shows a slow monotonic decrease with time. It decreases to one fourth of its initial value in about 150 Myr.

7.5. The star formation efficiency of collisional tori

Star formation in collisional disks is expected (see Sec. 3) to be proportional to the cloud collision rate \(\dot{M}_{\text{coll}} = \Omega/\vartheta\):

\[
\dot{M}_* = \eta M_{\text{gas}} \vartheta^{-1} \Omega,
\]

where \(\eta\) is the star formation efficiency which we would like to determine. This is only possible for Circinus, because only in this case the peak star formation rate derived from observations reflects the initial star formation rate of the collisional torus (scenario II). For all other AGNs the peak star formation rate is related to a massive \((Q \sim 1)\) turbulent gas disk. During the torus evolution at constant thickness (Phase II) the star formation rate is proportional to the square of the gas mass

\[
\dot{M}_* \propto M_{\text{gas}}^2.
\]

The initial and present gas mass of the torus in Circinus are \(M_{\text{gas}}^{\text{init}} = 3.4 \times 10^6\) M\(_\odot\) and \(M_{\text{gas}} = 2 \times 10^6\) M\(_\odot\); the peak star formation rate is \(\dot{M}_*^{\text{init}} = 0.02\) M\(_\odot\) yr\(^{-1}\). This leads to an estimate of the present star formation rate of \(\dot{M}_* = 7 \times 10^{-3}\) M\(_\odot\) yr\(^{-1}\). The resulting star formation efficiency is

\[
\eta = \frac{R \dot{M}_*^{\text{init}}}{M_{\text{gas}}^{\text{init}} \vartheta_{\text{rot}}} \simeq 10^{-3}.
\]

For a turbulent galactic disk the star formation law is

\[
\dot{M}_* = \eta_{\text{gal}} M_{\text{gas}} \Omega.
\]

Thus, one has to compare \(\eta/\vartheta \sim 5 \times 10^{-4}\) for a collisional disk with \(\eta_{\text{gal}} = 0.017\) derived for galactic SN driven turbulent gas disk. We conclude that the star formation in a collisional torus...
is about 10 times less efficient than that of a turbulent gas disk of the same mass. In our sample of 6 AGN the star formation rate of the present collisional torus is small compared to the mass accretion rate. The average fraction between the mass accretion rate and the star formation rate in these tori is $25 \pm 7$.

### 7.6. Obscuring the starburst

The stellar luminosities calculated by Davies et al. (2007; their Fig. 8) indicate that on scales of several tens of parsecs, the starbursts can only be weakly obscured. The reason for this is explained by Davies et al. (2006), and summarised here. If one assumes no obscuration, the starburst already comprises typically a few percent of the galaxy’s bolometric luminosity. Even a moderate optical depth will lead to nearly all the optical light being absorbed and re-radiated in the far-infrared; and in addition the scaling one derives for the starburst would increase. The limiting constraint is that the starburst luminosity cannot exceed the galaxy’s bolometric luminosity. We estimate the resulting extinction (for screen models) to be in the range $A_V = 4$ to 8. This is consistent with a clumpy torus with area filling factors below unity (transparency $\vartheta > 1$) for radii larger than about 1 pc. The optical extinction is then mainly due to dust located in the foreground of the star forming region. In Sy2 galaxies, however, not only the central AGN is obscured by the torus, but also the inner part of the torus and embedded star forming regions are self-obscured by the extended torus. To verify this idea, we use the model of Beckert & Duschl (2004) and Hönig et al. (2006) which is based on the formalism developed by Vollmer et al. (2004) to estimate the extinction using (i) a screen model where the starburst occurred in the torus midplane behind half the torus, and (ii) a mixed model where the forming stars and the clouds share the same spatial distribution within the torus. As an example we use parameters most appropriate for NGC 3227 or NGC 1068: $v_{turb}/v_{rot} = 0.55$, $\vartheta = 2$ with an outer radius of 80 pc. Fig. 3 shows the mean number of clouds $\Lambda$ along the line of sight through the torus for two torus inclinations in the case of a screen model.

$$\Lambda = \int l_{\text{coll}}^{-1} \, ds,$$

where $l_{\text{coll}} = \vartheta H$ is the mean free path of the clouds and $H$ the disk height. Obscuration with $\Lambda \geq 3$ leading to an likelihood of non-obscuration of less than $e^{-3}$ occurs at a radii $R \leq 20$ pc for $i = 60^\circ$ and not at all for $i = 40^\circ$. For lower inclinations the obscuration by clouds is ineffective. For $i > 60^\circ$ the obscuration pattern does not change much for geometrically thick tori.

Fig. 3 shows the ratio between the extinction-free starburst emission and the emission with obscuration by intervening clouds in the mixed case

$$\frac{I_0}{I_{\text{ext}}} = \frac{\Lambda}{1 - e^{-\Lambda}}.$$

Complete absorption $I_0/I_{\text{ext}} \gg 1$ is only reached in the innermost part of the AGN torus ($R \leq 1$ pc).

The screen and the mixed models can be regarded as two extreme cases and the reality maybe somewhere in between these two models. Most probably the starburst will be significantly obscured at galactocentric radii smaller than 1 pc. The extinction of star formation at the 10 pc scale by torus clouds is so low that additional extinction by extended dust lanes at larger radii ($> 100$ pc) in the galaxies is possible. We can therefore conclude that our torus model is consistent with the small observed extinction of the central starburst.

Fig. 3. Projected mean number of clouds $\Lambda$ along the line of sight through the torus for the screen model. Contour levels are (0.5,0.75,1.1,5,2,2.5,3,..). The thick contour is for $\Lambda = 1$ corresponding to an non obscuration probability of $e^{-1}$. Upper panel: torus inclination $i = 45^\circ$. Lower panel: torus inclination $i = 60^\circ$ ($i$ measured from the torus axis). The size of the box is 100 pc.
The inner edge of the torus is thought to be set by the dust sublimation radius which is located at about $i = 50^\circ$. Contour levels are (1.5, 2, 2.5). The thick contour is for $I_0/I_{\text{ext}} = 2$. It is the seconds outermost contour.

8. Fueling the central engine

The inner edge of the torus is thought to be set by the dust sublimation radius which is located at about 0.1-0.5 pc from the central black hole. In Sect. 7 we have derived the mass accretion rate onto the central black hole and what the relation is to the maser emission regions. These maser disks have sizes of about 0.1 pc. Between 0.1 pc and 0.5 pc from the central black hole an X-ray heated wind is most likely formed (Krolik & Kriss 1995, 2001). Less dense and sheared clouds lose their dust by evaporation at the sublimation temperature are consequently ionized by the AGN X-ray emission, heated, and blown away in a line-driven wind. What remains of the dust or is newly formed in the wind to the emission with cloud absorption $I_0/I_{\text{ext}}$ for an torus inclination of $i = 50^\circ$. Contour levels are (1.5, 2, 2.5). The thick contour is for $I_0/I_{\text{ext}} = 2$. It is the seconds outermost contour.

The inner edge of the torus is thought to be set by the dust sublimation radius which is located at about $i = 50^\circ$. Contour levels are (1.5, 2, 2.5). The thick contour is for $I_0/I_{\text{ext}} = 2$. It is the seconds outermost contour.

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The inner edge of the torus is thought to be set by the dust sublimation radius which is located at about $i = 50^\circ$. Contour levels are (1.5, 2, 2.5). The thick contour is for $I_0/I_{\text{ext}} = 2$. It is the seconds outermost contour.
cloud radius does not change with the cloud’s distance from the galactic center.

We scale up the Galactic Center by a factor of $10^4$ and obtain $c_1 = 7.6 \text{ km s}^{-1}$, $c_5 = 3 \text{ km s}^{-1} (R/(1 \text{ pc}))^{-\frac{1}{2}}$, and $J_{\text{UV}} = 1.8 \times 10^{16} \text{ cm}^{-2} \text{s}^{-1} (R/(1 \text{ pc}))^{-2}$ for a transparent torus. This leads to a cloud radius of $r_{\text{cl}} = 0.03 \text{ pc}$, which is very close to the cloud radius obtained for our sample of AGN tori (Table 4). Thus, only dense, self-gravitating clouds can survive in an illuminated environment, i.e. a transparent torus. On the other hand, if the torus is opaque, less dense and larger clouds can survive. Since we derive only the properties of the densest and most massive clouds in our model which determine the physics of the outer torus, less dense and less massive clouds are still consistent with the model as long as they do not dominate the disk mass. As a consequence, the transparency values derived for the individual AGNs and summarized in Table 4 are upper limits. We therefore suggest that towards the inner edge of opaque tori clouds become less dense with densities close to the shear limit. These clouds, however, once they arrive at the inner edge of the torus, are (i) destroyed easily by the influence of shear and possible winds and (ii) are much ionized and evaporated by the AGN emission. In addition, for AGN close to the Eddington limit Hönig & Beckert (2007) showed that dusty clouds experience a strong radiation pressure. For transparent tori only dense and compact clouds smaller than the shear limit will be found, while for opaque tori shadowing by clouds at the inner edge allows larger clouds to survive at intermediate distances.

This tentative picture leads to two predictions for AGN tori that might be verified in the future:

- the inner parts of opaque tori should harbor larger clouds and should therefore have larger volume filling factors,
- the ratio of the torus mass accretion rate to the mass removed in winds generated at the inner boundary of tori should be lower for opaque tori.

9. Uncertainties

Up to this point we ignored any possible observational errors. In this section the influence of the quantities derived from observations on the correlations shown in Fig. 2 and Fig. 5 is investigated. We assume the following uncertainties:

- For the gas mass ($M_{\text{gas}}$) - about a factor 2, because of the uncertainty in mass distribution and hence in interpreting the kinematics;
- peak star formation rate ($M_\star^{\text{peak}}$) - at least a factor 2-3 since the extinction is not well constrained;
- starburst age ($t_{\text{SB}}$) - up to a factor 2, assuming that all diagnostics are explained by a single burst, which we reject for NGC3783;
- rotation velocity ($v_{\text{rot}}$) - $\sim 40 \%$, since it is the equivalent Keplerian rotation velocity, and depends on both the measured dispersion and inclination-corrected velocity;
- turbulent velocity dispersion ($v_{\text{turb}}$) - $\sim 20 \%$ assuming that the velocity dispersion is not strongly affected by a wind.

All uncertainties of our derived quantities are thus dominated by the observational uncertainties on $M_{\text{gas}}$ and $M_\star$. For the torus mass accretion rate we have

$$
M = \frac{128}{\pi^3} f_{\text{turb}} v_{\text{rot}}^{-2} M_\star^{2} M_{\text{dyn}}^{-2} \Omega r_{\text{cl}} . \tag{51}
$$

During the torus evolution the mass accretion rate is proportional to the square of the gas mass $M \propto M_{\text{gas}}^2$. The gas mass of the massive ($Q \sim 1$) turbulent disk only depends on the peak star formation rate

$$
M_{\text{gas}} \propto \left( M_\star^{\text{peak}} \right)^{\frac{2}{3}} . \tag{52}
$$

We took this gas mass as the initial gas mass of the collisional torus at the beginning of Phase II. Thus the ratio between the mass accretion rate of the present torus $M$ and that of the initial collisional torus $M_{\text{old}}$ (Fig. 2) depends on the square of the present gas mass $M_{\text{gas}}$ and on the inverse of the peak star formation rate $M_\star^{\text{peak}}$.

$$
\frac{M}{M_{\text{old}}} \propto \frac{M_{\text{gas}}^2}{M_\star^{\text{peak}}} . \tag{53}
$$

On the other hand, the ratio between the mass accretion rate onto the black hole $M_{\text{BH}}$ and the torus mass accretion rate $M$ depend on the AGN luminosity $L$ and on the inverse of the square of the gas mass $M_{\text{gas}}$:

$$
\frac{M_{\text{BH}}}{M} \propto \frac{L}{M_{\text{gas}}^2} . \tag{54}
$$

An underestimation of the gas mass, which we assumed to be 10% of the dynamical mass, thus leads to a strong increase of the two ratios, while an underestimation of the peak star formation rate and the AGN luminosity leads to a decrease of the two ratios. In extreme cases both ratios can have errors up to a factor of 10.

The starburst ages have uncertainties of a factor of 2. The area filling factor is proportional to the inverse of the gas mass $\Phi_V \propto M_{\text{gas}}^{-1}$ (Eq. 55). Thus, the associated uncertainty is also a factor of 2.

Despite these relatively large uncertainties we believe that the correlations shown in Fig. 2 and 5 are real. All systematic errors, like an overestimate of the gas mass, would alter but not destroy the correlations, as long as the errors for different targets are not random. However, to make our findings more robust we need high spatial resolution of AGNs. Most importantly, future ALMA high resolution CO line observations are necessary to determine the total gas mass of the tori with an uncertainty of $\sim 10 - 30 \%$.

10. A holistic view of torus evolution in AGN

VLT SINFONI observations of the close environments ($\sim 30 \text{ pc}$) of a sample of nearby AGNs by Davies et al. (2007) showed that thick gas tori and recent central starbursts with ages smaller than 100 Myr are ubiquitous. We compare different clumpy accretion disk models to these observations:
fully gravitational turbulent disks where the turbulence is maintained by the energy input from the gravitational potential via mass accretion,

- supernova and stellar wind driven turbulent disks (SN model) where the turbulence is maintained by stellar winds and supernova explosions,

- collisional disks where the orbital motion is randomized by partially elastic collisions which also allow mass transport to the center and angular momentum redistribution.

Whereas the measured rotation velocity, turbulent velocity dispersion, and gas mass tell us about the current state of the gas torus, the peak star formation rate and the age of the starburst provide information on the past appearance of the torus. We assume that the physical properties of the torus are mainly determined by external mass accretion from scales of \( \sim 100 \) pc.

The result of this work is a time sequence for the torus evolution. Present tori appear to be collisional and geometrically thick whereas the tori giving rise to the starburst in the past are of turbulent nature and relatively thin. The torus evolution can be divided into 3 phases depending on the external mass accretion rate:

- **Phase I**: initial massive infall: formation of a massive turbulent stellar wind-driven gas disk with \( Q \sim 1 \),

- **Phase II**: decreasing, but still high mass accretion rate: collisional thick torus,

- **Phase III**: decreasing, now low mass accretion rate: collisional thin torus.

Phase I is short (\( \sim 10 \) Myr). Once the SN explode, they remove the intercloud medium and clear the disk leaving behind only the densest clouds. The result is a collisional torus. All tori discussed in this paper are interpreted to be in phase II. Therefore this phase can last for more than 100 Myr. The transparency of these tori depend on their Toomre parameter, the turbulent velocity, and the internal pressure of the clouds (temperature and magnetic fields). If there is a second short massive infall, the torus can again switch into phase I. We suggest that this has happened in the case of NGC 3783. On the other hand, an initial massive gas infall is not mandatory as the case of Circinus illustrates. Once the external mass accretion rate has significantly decreased, the torus becomes thin and transparent. The Circumnuclear Disk in the Galactic Center represents this phase.

In addition we conclude that

1. The massive turbulent stellar wind-driven gas disk (phase I) gives rise to a starburst with a star formation rate that equals the disk mass accretion rate.

2. The collisional torus also forms stars, but with an efficiency which is about 10% that of the turbulent disk.

3. During the evolution of the thick collisional torus (phase II) the decrease of the mass accretion rate is slow (a factor of 4 within 150 Myr).

4. The present collisional tori (phase II) do not significantly obscure the stellar populations born during the recent starburst. This is the case even for Sy2 nuclei.

5. We find a tentative correlation between the area filling factor of the clouds and the ratio between the mass accretion rate onto the central black hole and the torus mass accretion rate. AGNs with a high area filling factor lose more than 90% of the mass transported through the torus in a thermal torus wind at the inner edge. We suggest that this is due to shadowing of the gas clouds from the central AGN throughout most the extended torus which allows the existence of low density clouds whose densities are close to the shear limit.

Future VLT SINFONI and ALMA observations will be necessary to confirm our proposed torus evolution sequence.

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