Extraction of neutrino Yukawa parameters from displaced vertices of sneutrinos

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Abstract: We study displaced signatures of sneutrino pairs potentially emerging at the Large Hadron Collider (LHC) in a Next-to-Minimal Supersymmetric Standard Model supplemented with right-handed neutrinos triggering a Type-I seesaw mechanism. We show how such signatures can be established through a heavy Higgs portal, the sneutrinos then decaying to charged leptons and charginos giving rise to further leptons or hadrons. We finally illustrate how the Yukawa parameters of neutrinos can be extracted by measuring the lifetime of the sneutrino from the displaced vertices, thereby characterising the dynamics of the underlying mechanism of neutrino mass generation. We show our numerical results for the case of both the current and High-Luminosity LHC.

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1 Introduction

The Standard Model (SM) has survived nearly all experimental tests. Besides the strong evidence for Dark Matter (DM), the only unexplained experimental phenomenon is neutrino oscillations [1–6], which in turn imply that neutrinos have a tiny, but non-zero, mass. The standard explanation is that neutrino masses are generated through a seesaw mechanism [7–12], where the effective dimension five operator responsible for neutrino masses is suppressed by a heavy mass scale.

The range of possible seesaw scales varies from eV-scale sterile neutrinos to those with masses of the order $10^{14}$ GeV. Taking type-I seesaw as an example, the neutrino Yukawa couplings are $\mathcal{O}(1)$ at the upper end while they are tiny at the lower end of the possible spectrum of their interaction strength. One interesting option is that the seesaw scale is around the Electro-Weak scale (EW), which requires the neutrino Yukawa couplings to be somewhat smaller than the electron Yukawa coupling. As the Right-Handed (RH) neutrinos are singlets under the SM gauge group, the only interactions they have are the Yukawa couplings, which being small can lead to Displaced Vertices (DVs) [13–17].

Supersymmetry (SUSY) is a well-motivated framework for Beyond the SM (BSM) physics. SUSY is the only space-time symmetry that can be added to the Poincaré algebra [18] and it relates particles with different spins, specifically, bosons to fermions. This relation leads to the cancellation of quadratic divergences emerging in the calculation of the Higgs boson mass in the SM (the so-called hierarchy problem). Furthermore, SUSY may induce the convergence of the Electro-Magnetic (EM), weak and strong couplings at some high energy scale, unlike the SM, a precondition for a theory embedding unification.
of forces. Finally, if one removes the baryon and lepton number violating couplings by requiring \( R \)-parity, one can get as a by-product of SUSY a DM candidate in the form of the Lightest Supersymmetric Particle (LSP).

Needless to say then, in order to pursue BSM physics that addresses all the aforementioned SM flaws, SUSY is one of the possible paths to follow, so long that it embeds a mechanism for neutrino mass generation. In doing so, it is then necessary to surpass its minimal realisation and consider non-minimal ones \([19]\), wherein the gauge and/or Higgs structures are enlarged with respect to the case of the Minimal Supersymmetric Standard Model (MSSM). An attractive framework in this respect is the Next-to-MSSM (NMSSM), wherein a singlet Superfield, containing an extra singlet Higgs state and its SUSY counterpart, is added to the MSSM particle content. This way, the so-called \( \mu \)-problem \([20]\) of the MSSM is overcome. If such a construct is supplemented with RH neutrinos and their SUSY counterparts, a viable model for neutrino mass generation based on a type-I seesaw is established.

By adopting this theoretical framework, we will show that the heavy Higgs states belonging to it (both CP-even and -odd) can have significant couplings to RH sneutrinos, even in the alignment limit, as required by measurements of the SM-like Higgs boson discovered at the Large Hadron Collider (LHC) in 2012. Furthermore, given that in this model RH (s)neutrinos and higgsinos get their masses through the same mechanism, one can expect the SUSY states to be rather degenerate, yet, suitable soft SUSY-breaking mass terms can render the RH sneutrinos somewhat heavier than the higgsinos. In such a case a RH sneutrino can decay visibly through its Yukawa interactions to a charged lepton \((\ell = e, \mu)\) and chargino or else a neutrino and neutralino. Therefore, a typical signal that may emerge at the LHC in this theoretical scenario is heavy Higgs mediated production of a sneutrino pair eventually yielding a di-lepton signature together with soft jets and missing transverse energy. As the seesaw mechanism has a source of lepton number violation, we get both opposite-sign and same-sign dileptons, the latter giving better discovery potential due to smaller backgrounds. Remarkably, the aforementioned mass degeneracy may make the sneutrinos long lived, so that the visible tracks of this signature may be displaced, which in turn implies a smaller background with respect to the one affecting similar prompt signatures \([21, 22]\). Here we shall prove that this signature with two DVs can be extracted at the LHC and, moreover, we shall also show how the kinematics of the displaced (visible) tracks could allow for a measurement of the (s)neutrino Yukawa couplings, thereby enabling one to probe the underpinning neutrino mass generation dynamics.

Our paper is organised as follows. In the next section we introduce our theoretical framework. In the following one we illustrate the properties of the track displacements and how these can be related to the discussed Yukawa couplings. Then we perform our MC analysis aimed at extracting both the relevant signature and its underlying (s)neutrino mass parameters. We then conclude.
2 NMSSM with RH neutrinos

We shall study the NMSSM with RH neutrinos. It is based on the following Superpotential [23, 24]

\[ W = y_{u ij} (Q_i \cdot H_u) U_j^c - y_{d ij} (Q_i \cdot H_d) D_j^c + y_{\nu ij} (L_i \cdot H_u) N_j^c + \lambda S (H_u \cdot H_d) + \frac{\lambda N_i}{2} S N_i^c N_j^c + \frac{\kappa}{3} S^3. \] (2.1)

As mentioned, this model cures some problems of the MSSM, namely the $\mu$-term will be generated through the Vacuum Expectation Value (VEV) of the scalar component of the singlet Superfield $S$ and we also have a mechanism for neutrino mass generation. As the $\mu$-term should not be too far above the EW scale, the RH neutrino masses are at the EW scale too, hence the neutrino Yukawa couplings need to be very small, of the order $10^{-7}$.

We shall look at a scenario where we have light higgsinos and RH neutrinos being roughly degenerate with these. The soft SUSY-breaking masses should then make the RH sneutrinos heavier than the higgsinos and thus the decays $\tilde{N} \rightarrow \tilde{\chi}_0^0 \nu, \tilde{\chi}_\pm \ell^\mp$ are kinematically open. The decay width will be given by the neutrino Yukawa couplings. As mentioned, they will be tiny, and thus may lead to DVs.

This model allows two important features: EW Symmetry Breaking (EWSB) generates both a lepton-number violating mass term for the RH sneutrinos and a coupling between Higgs states and the sneutrinos. The coupling in the alignment limit is (neglecting doublet-singlet mixing)

\[ C_{h \tilde{N}} = \pm \frac{1}{2} \lambda_N v \sin 2\beta, \] (2.2)
\[ C_{H \tilde{N}} = \pm \frac{1}{2} \lambda_N v \cos 2\beta, \] (2.3)

where the upper (lower) sign is for CP-even (CP-odd) sneutrinos. If $\tan \beta > 1.5$, the heavy Higgs state has a stronger coupling to sneutrinos. If $\lambda$ and $\lambda_N$ are large, RH sneutrinos can be pair produced through the heavy Higgs portal and they can be detected through lepton-number violating signatures [21, 22]. The singlet field is essential in achieving this as in the MSSM with RH neutrinos the Higgs-RH sneutrino couplings would not exist. As intimated, our aim is to use DVs to both improve background rejection and allow for a quantitative estimate of the neutrino Yukawa couplings.

3 From displacements to Yukawa couplings

We shall assume that the only kinematically available decay channels for the sneutrino are $\tilde{N} \rightarrow \tilde{\chi}_0^0 \nu, \tilde{\chi}_\pm \ell^\mp$ and that the neutralino and chargino are higgsino-like.

The sneutrino-lepton-chargino vertex factor is

\[ \lambda_{\tilde{N} \ell^+ \tilde{\chi}^-} = \frac{i}{\sqrt{2}} y_{\nu ab} V_{12} \left( 1 + \gamma_5 \right), \] (3.1)

where $a, b$ refer to the flavours of the charged lepton, sneutrino and $V_{12}$ tells the higgsino component of the lightest chargino. For CP-odd sneutrinos we only need the replacement
\[ \sqrt{2} \to \frac{1}{\sqrt{2}}. \] This leads to the partial width (neglecting the lepton mass)

\[ \Gamma(\tilde{N}_i \to \ell_j^\pm \tilde{\chi}^\mp) = \frac{(m_{\tilde{N}}^2 - m_{\tilde{\chi}}^2)^2}{16\pi m_{\tilde{N}}^2} |y_{ji}|^2 |V_{12}|^2. \tag{3.2} \]

We shall assume |V_{12}| = 1 in the following.

If we neglect the mixing between Left-Handed (LH) and RH neutrinos,\(^1\) the sneutrino-neutrino-neutralino vertex factor is

\[ \lambda_{\tilde{N}Nj5} = -\sum_i \sqrt{2} \left( N_{ij}^* P_{abc} y_{bc}^\nu \frac{1 - \gamma_5}{2} + N_{ij} P_{abc} y_{bc}^\nu \frac{1 + \gamma_5}{2} \right), \tag{3.3} \]

where \( P \) is the Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix, \( b \) and \( c \) are the flavours of the neutrino and sneutrino, respectively, while \( N_{ij} \) gives the \( \tilde{H}_u \) component of the neutralino \( j \). For CP-odd sneutrinos we shall again replace \( \sqrt{2} \to \frac{1}{\sqrt{2}} \) in the prefactor. This gives the partial width

\[ \Gamma(\tilde{N}_i \to \nu_j \tilde{\chi}_0^j) = \sum_k \frac{(m_{\tilde{N}}^2 - m_{\tilde{\chi}_0}^2)^2}{16\pi m_{\tilde{N}}^2} |y_{kj}|^2 |N_{j3}|^2. \tag{3.4} \]

Here \( j \) can get values 1, 2 and \( |N_{j3}|^2 \simeq 1/2 \).

From Equations (3.2) and (3.4) we see that the total decay width is proportional to \( \sum_i |y_{ij}|^2 \). Hence the measurement of the lifetime of the sneutrino will give an estimate of the sum of the Yukawa couplings, while the ratios \( |y_{jk}/y_{jk}|^2 \) are proportional to \( \text{BR}(\tilde{N}_k \to \ell_i^\pm \tilde{\chi}^\mp)/\text{BR}(\tilde{N}_k \to \ell_j^\pm \tilde{\chi}^\mp) \). Measuring the lifetime and the ratios of the Branching Ratios (BRs) would then give us the absolute values of the individual neutrino Yukawa couplings.

We shall assume that the chargino and neutralinos would have been observed already and their masses would be known reasonably well. From the decay mode \( \tilde{N} \to \ell^\pm \tilde{\chi}^\mp \) and the subsequent chargino decay \( \tilde{\chi}^\pm \to \tilde{\chi}_0^0 \) hadrons, the invariant mass of the visible decay products should have an endpoint at \( m_{\tilde{N}} - m_{\tilde{\chi}_0} \) from which the sneutrino mass could be estimated. We also expect that the mass of the heavy Higgs bosons would be known from one of its fermionic decay modes.

In order to extract the lifetime of the sneutrino in its rest frame, we need to measure the position of the secondary vertex and the relativistic \( \gamma \)-factor of the sneutrino, which can be computed, e.g., through \( \gamma_{\tilde{N}} = E_{\tilde{N}}/m_{\tilde{N}} \). This can be done on an event-by-event basis as follows.

In the Center-of-Mass (CM) frame energy-momentum conservation gives us

\[ E_{\tilde{N}}^* = \frac{m_H}{2}, \tag{3.5} \]

\[ p_{\tilde{N}}^* = \sqrt{\frac{m_H^2}{4} - m_{\tilde{N}}^2}. \tag{3.6} \]

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\(^1\)This mixing introduces a vertex factor \( \lambda_{Nj5} \) times the RH neutrino component of the light eigenstates. The elements of the neutrino left-right mixing matrix are of the same order as the elements of \( y^\nu \). As the singlino component \( N_{j5} \) is not negligible, this correction to the vertex factor is numerically only an order of magnitude smaller than \( |y^\nu N_{j5}| \) so this does introduce an \( \mathcal{O}(10\%) \) correction to the partial width.
Figure 1. The kinematics can be solved as shown. As the sneutrinos are neutral, their momentum vectors are aligned with the displacements of the secondary vertices from the primary vertex. We then construct the momenta in the lab frame by using these direction vectors and the fact that the transverse components are equal. Then we may boost to the center-of-mass frame, where we know the total momentum $p^*$ drom eq. (3.6).

To figure out what are the sneutrino momenta in the laboratory frame, we may use the following facts.

- The initial transverse momentum of the heavy Higgs boson is nearly zero as long as there are no hard prompt jets in the event.

- The three-momentum of the sneutrino is directed from the primary vertex to the secondary one, since the sneutrino is a neutral particle and its trajectory will not be curved.

We shall draw vectors from the primary vertex to the secondary vertices as shown in figure 1. Next we shall scale them so that $|p_{T,S_1}| = |p_{T,S_2}|$ based on the small initial transverse momentum. Due to the difference of initial state gluon momenta, the final state will have a net momentum in the $z$-direction, but we may boost to the CM frame simply.
by adding equal vectors to both laboratory frame momenta. Once we are in the CM frame, we know $p_N^*$ from Equation (3.6) and hence may solve for $p_{T, N}$. This then allows us to compute

$$p_{N} = p_{T, N} \sqrt{1 + \frac{d_z^2}{d_\perp^2}},$$

(3.7)

where $d_z$ and $d_\perp$ are the longitudinal and transverse displacements, respectively. In figure 2, we show a representative image of the trajectory of a long-lived particle in a 2-dimensional plane (from [25]).

We can then deduce $E_N = \sqrt{p_N^2 + m_{\tilde{N}}^2}$ and from this $\gamma_N$. As the total displacement is

$$d = \gamma_N v \tau,$$

(3.8)

where $v$ is the velocity and $\tau$ the lifetime of the sneutrino, we may solve for the lifetime

$$\tau = \frac{d}{\gamma_N \sqrt{1 - \frac{1}{\gamma_N^2}}},$$

(3.9)

The lifetimes follow an exponential probability distribution

$$P(\tau) \propto e^{-\tau/\tau_0},$$

(3.10)

where $\tau_0$ is the average lifetime. Plotting the lifetime distribution with a suitable binning with a logarithmic scale should then produce a straight line, whose slope gives the inverse of the average lifetime.\(^2\)

When Next-to-Leading Order (NLO) and even higher order corrections are taken into account, the Higgs bosons will have a finite initial transverse momentum $p_H^T$. This will introduce a relative error in the measurement of the momenta, which is of the order of $p_H^T/p_{\tilde{N}}$. As we are interested in events that do not have a large longitudinal boost, i.e., all decay products are in the barrel region of the detector, we expect typically the $\gamma$-factor of the sneutrino to be rather small. In such a case the error on $\gamma_N$ will be of the order of

\(^2\)We refer to [26, 27] for elaborated discussions on determining the lifetime of long-lived particles at the LHC.
\( (p_T^H/m_\tilde{N})^2 \). If we veto for hard jets a typical \( p_T^H \) is about 10 GeV \cite{28} and the mass of the sneutrino is 200 GeV or more so the error from the finite initial transverse momentum on the lifetime measurement is very small.

4 Collider analysis

We shall look at the process \( pp \to H, A \to \tilde{N}\tilde{N} \), where both sneutrinos decay visibly giving a charged lepton (\( \ell = e, \mu \)) and a charged higgsino. In this model the sneutrinos do not have a well-defined lepton number and the lepton number violating mass splitting is larger than the decay width, so there is a 50% chance for each sneutrino to decay to either charge lepton. As the backgrounds for same-sign dileptons are smaller, we choose events with two same-sign leptons and veto for a third hard lepton with \( p_T > 15 \) GeV.

If the higgsinos have a relatively smaller mass splitting, say close to 5 \(- 10\) GeV, then the decay width for the sneutrino to visible decays is small. Numerically the minimal width is close to \( 10^{-14} \) GeV leading to a mean decay length of a couple of millimeters. In contrast, in the region of phase space where the production of heavy Higgses is possible with a reasonable cross section and the decays are kinematically allowed, the decay widths are typically a few times \( 10^{-13} \) GeV. This implies that the mean decay lengths are around hundreds of micrometers, which leads to final states with DVs. Thus for a large fraction of the signal events we should have two DVs with charged leptons and soft charged tracks.

In this work, we require both of the leptons (\( \ell = e, \mu \)) to be displaced. Such a requirement means that the backgrounds come from processes involving either \( b \)-quarks or \( c \)-quarks. The same-sign requirement further reduces these as in the case of only two heavy-flavour quarks same-sign leptons are possible only in the case of flavour oscillations.

Our signal events will have missing transverse momentum in the form of the LSPs and, if the spectrum is not compressed, it is possible to require large \( \not{p}_T \) with a rather good signal acceptance. Heavy flavour events rarely satisfy this requirement. In order to have neutrinos with significant transverse momentum, the quarks in the hard process must have large \( p_T \) and the cross section falls down quickly with increasing \( p_T \). Also, \( t\bar{t} \) events with both the tops decaying hadronically can kinematically mimic the signal events.

4.1 Event generation procedure

For detailed analysis we choose the three Benchmark Points (BPs) given in table 1. While they differ slightly in their mass spectrum, their main difference is in the sneutrino lifetimes. BP-I represents a “typical” benchmark for EW scale seesaw with a decay width corresponding to a mean decay length around 1 mm. The second benchmark has a shorter lifetime with a mean decay length less than 0.3 mm, while the third one has a mean decay length around 2 mm, which is about as long as one can get without going to very compressed spectra. For such cases any leptons would be soft and triggering the event would be more difficult. For interested readers, we refer \cite{29, 30} for the recent proposals on these issues.

Regarding the constraints on the spectrum, the higgsinos need to be heavier than about 160 GeV with a mass splitting of 10 GeV \cite{31}. Since \( m_H > 2m_{\tilde{N}} > 2m_\tilde{H} \), the heavy
Higgses need to be beyond 400 GeV. However, the production cross section falls off rather quickly beyond 500 GeV. In this range $\tan\beta$ needs to be low to avoid the constraints from $H \rightarrow \tau^+\tau^-$ searches [32, 33]. For our BPs we have $2 < \tan\beta < 3$ as this both evades the experimental constraints and gives a large $\text{BR}(H \rightarrow \tilde{N}\tilde{N})$.

We simulate 100,000 signal events and $\mathcal{O}(10^7)$ events each for the $t\bar{t}$ and $b\bar{b}$ backgrounds using MadGraph5 v2.6.6 [34] at LO. Parton showering and hadronisation are modelled through Pythia v8.2 [35] and fast detector simulation is obtained by Delphes v3.3.3 [36] with the ATLAS card. We use a modified version of the default ATLAS card to implement the impact parameter smearing effects. The event rates are then corrected to NLO accuracy with $k$-factor of 2 for the signal [37–39] and to next-to-next-to-leading order (NNLO) accuracy with $k$-factor of 1.8 for the two dominant backgrounds [40–42].

Further, in order to generate events efficiently, we demand that the top quarks are decaying hadronically and the $b$-hadrons, obtained after parton shower and hadronisation of the $b$-quarks, are decaying through leptonic final states. We generate two sets of $b\bar{b}$ samples by varying the $p_T$ of the bottom quarks at the generation level. We find that the one with generation level cut $p_T^{b,\text{min}} = 200$ GeV has better sensitivity. In table 2, we show the details of event generation of individual signal and background events.

Note that, as pointed out in ref. [42], at high transverse momenta of the bottom quarks, large logarithmic terms of the form $\ln\left(\frac{p_T^{b}}{m_b}\right)$ become important and need to be resummed properly while estimating the NNLO cross section for the $b\bar{b}$ process. For our study, bottom quarks are pair produced with a minimum $p_T^{b} = 200$ GeV, so we make a conservative choice of $k$-factor = 1.8.

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**Table 1.** Details of the BPs (all the masses are in GeV). The leptonic BRs include electron, muons and taus.

| Observable | BP-I | BP-II | BP-III |
|------------|------|-------|--------|
| Lightest Higgs mass | 125.0 | 125.2 | 125.6 |
| 2nd Higgs mass | 338.2 | 322.1 | 370.4 |
| 3rd Higgs mass | 462.2 | 484.0 | 483.6 |
| Lightest Pseudoscalar Higgs mass | 259.0 | 256.8 | 261.7 |
| 2nd Pseudoscalar Higgs mass | 446.9 | 470.2 | 468.1 |
| Lightest Sneutrino mass | 219.4 | 219.9 | 228.4 |
| Lightest CP-odd Sneutrino mass | 185.8 | 177.6 | 205.1 |
| Lightest Chargino mass | 185.3 | 168.2 | 196.0 |
| Lightest Neutralino mass | 200.3 | 193.2 | 218.6 |
| $\text{BR}(h_3 \rightarrow \tilde{\nu}_1 \tilde{\nu}_1) \ (\text{in \%})$ | 5.3 | 4.9 | 4.9 |
| $\text{BR}(A_3 \rightarrow \tilde{\nu}_1 \tilde{\nu}_1') \ (\text{in \%})$ | 1.2 | 1.3 | 1.6 |
| $\text{BR}(\tilde{\nu}_1 \rightarrow \ell \tilde{\chi}^0_1)$ \ (\text{in \%}) | 48.2 | 48.6 | 45.3 |
| $\text{BR}(\tilde{\nu}_1 \rightarrow \nu \tilde{\chi}^0_1)$ \ (\text{in \%}) | 51.8 | 51.4 | 54.7 |
| $\Gamma(\tilde{\nu}_1) \ (\text{GeV})$ | $1.6 \times 10^{-13}$ | $8.5 \times 10^{-13}$ | $9 \times 10^{-14}$ |
| Process                          | Cross section (pb) | Events generated | Event weight factor |
|---------------------------------|--------------------|------------------|--------------------|
| Signal (BP-I)                   | 0.0666             | 100,000          | 0.09               |
| Signal (BP-II)                  | 0.0558             | 100,000          | 0.08               |
| Signal (BP-III)                 | 0.0508             | 100,000          | 0.07               |
| $t\bar{t}$ (hadronic)           | 369.0              | 10,000,000       | 5.1                |
| $b\bar{b}$ ($p_T^{b_{\text{min}}} = 30\text{GeV}$) | 1183654.3          | 5,000,000        | 32432.1            |
| $b\bar{b}$ ($p_T^{b_{\text{min}}} = 200\text{GeV}$) | 378.0              | 10,000,000       | 5.2                |

**Table 2.** Event simulation details at $\sqrt{s} = 13$ TeV and $L = 137 \text{ fb}^{-1}$.

### 4.2 Definition of displaced objects

We now provide the details of the observables used to probe the displaced signal events.

- **Displaced leptons**: the isolated leptons ($\ell = e, \mu$) with $p_T(\ell) > 10\text{ GeV}$ and $|\eta(\ell)| < 2.5$ must satisfy $|d_\perp| > 0.2$ mm [43, 44] where $d_\perp$ is the transverse impact parameter relative to the primary vertex. The lepton isolation is achieved by demanding the angular separation between the lepton and jets, $\Delta R(\ell, \text{jet})$, should be greater than 0.4. Additionally, we demand that the leptons carry at least 80% (90%) of the transverse momentum within a cone of radius $R = 0.5$ in case of a muon (electron). Note that, we have used a modified version of the default ATLAS card available within Delphes to implement the impact parameter smearing effects and obtain the displaced leptons.

- **DV**s using displaced tracks**: the tracks used in the DV reconstruction must satisfy the following requirements: $p_T > 1\text{ GeV}$ and $|d_\perp| > 2$ mm. Further, the significance of $d_\perp$ with respect to the beam axis (i.e., $|d_\perp|$ divided by its uncertainty $\sigma_{d_\perp}$) should be at least 4 [44–46]. The final requirement on track $|d_\perp|/\sigma_{d_\perp}$ improves the identification of displaced tracks associated to the DVs.

We collect the displaced tracks and construct the DV. To combine the tracks, we use the truth information of the vertices (i.e., vertex position) obtained from the detector emulator and merge those tracks if $|\Delta X(t_i, t_j)| < 0.001$, $|\Delta Y(t_i, t_j)| < 0.001$ and $|\Delta Z(t_i, t_j)| < 0.001$, where $t_i$ denotes the $i$-th displaced track. The invariant mass of the DVs are calculated using the summed 4-momenta of the associated tracks, i.e., $m_{\text{DV}}^2 = (\sum E_i)^2 - (\sum \vec{p}_i)^2$, where the sum runs over the tracks associated to the DV [46].

- **Jets and displaced jets**: the jets are constructed from calorimeter tower elements using Fastjet v3.3.2 [47] and the anti-$k_T$ jet clustering algorithm [48] with jet radius $R = 0.5$. We demand that the jets must satisfy $p_T > 20\text{ GeV}$ and $|\eta| < 3.0$. For signal events, hadronic decay of the charginos leads to displaced hadronic final states. Note that long-lived hadrons (e.g., $b$-hadrons, $c$-hadrons) as well as soft particles coming from the prompt decay of the displaced hard processes are also present in the
events. So, we calculate the angular separation $\Delta R$ between the jet and the displaced tracks then demand that the displaced jet should have at least 2 or more displaced tracks satisfying $\Delta R(j, t) < 0.4$. The displaced jets are constructed following the refs. [49, 50]. We check that for signal events, the final state stable objects are not energetic enough to pass the jet $p_T$ threshold and provide significant separation from the background events, therefore, we do not consider the displaced jets for further analysis.

4.3 Distribution of different observables

Here we show the distribution of several kinematic variables relevant for the collider analysis. All the histograms are drawn for events which satisfy the basic selections on the leptons and jets discussed in the previous section. Distributions are scaled for $\mathcal{L} = 137$ fb$^{-1}$ of integrated luminosity at the $\sqrt{s} = 13$ TeV run of the LHC.

In the left panel of figure 3, we show the multiplicity of isolated leptons present in the signal and background events. The right panel displays the same distribution but for the isolated displaced leptons with minimum transverse impact parameter $d_{\perp} > 0.2$ mm. The $d_{\perp}$ distribution of the leading (in $p_T$) two leptons are shown in figure 4. Significant overlap is overserved especially at small values of $d_{\perp}$. As mentioned in the previous section, we construct the DVs using the displaced tracks and calculate the mass of the DV. In figure 5, we plot the mass of the leading (in mass) DV. It is evident that the presence of high $p_T$
displaced tracks, associated with the displaced leptons originating from the sneutrino decay, results in DVs with relatively larger masses. Therefore, we can control the background events by selecting events with mass greater than 5 GeV or so. Also, the distribution has a kinematical endpoint at $m_{\tilde{N}} - m_{\tilde{\chi}^{\pm}}$ so this can be used to estimate the sneutrino mass once the chargino mass is known.

4.4 Event selection and signal significance

After looking at the distributions of several kinematic observables, we find the following selection cuts optimised for our process of interest. The cuts are as follows.

- C1: two same-sign same-flavour leptons (electron or muons) satisfying basic lepton selection criteria.
- C2: the leading (in $p_T$) lepton must satisfy $p_T(\ell_1) > 25$ GeV.
- C3: the subleading (in $p_T$) lepton must satisfy $p_T(\ell_2) > 15$ GeV.
- C4: veto on a third lepton with $p_T(\ell_3) > 15$ GeV.
- C5: for opposite sign same flavour leptons, veto di-lepton invariant masses around the $Z$ mass i.e., $m_{\ell^+\ell^-} \neq [80, 100]$ GeV.
- C6: select events with $p_T > 30$ GeV.
- C7: both leptons have a transverse impact parameter $d_\parallel > 0.2$ mm.

Even though our main backgrounds are from heavy-flavour jets, in this study we did not want to impose a $b$-veto so that we would be free of uncertainties related to the $b$-tagging when we show the viability of our approach. As the displacement of a secondary vertex is a key input for $b$-tagging algorithms, the background displacement distributions would be affected by imposing a $b$-veto. Also the acceptance of the signal events is uncertain. If experimental collaborations were to do this type of an analysis, they may be able to further improve the background rejection with the use of a $b$-tagger.

The complete cutflow is presented in table 3. The signal significance ($\frac{S}{\sqrt{S+B}}$), calculated at $\sqrt{s} = 13$ TeV and $\mathcal{L} = 137$ fb$^{-1}$, is shown in table 4. We may see that the
displacement requirement rejects almost all of the signal of BP-II. For such a case the prompt signature can still be visible — this is actually BP3 of [21] for which a cut-based analysis gave a \( \sim 3\sigma \) excess. From table 3 it is interesting to note that even though the cuts C4 and C5 do not reduce the dominant backgrounds, however, they are important to reduce the sub-dominant backgrounds like WZ, ZZ, tW, tZ and \( t\bar{t}Z \) processes where both prompt and displaced leptons can be present.

Before we proceed to extract neutrino Yukawa couplings, we discuss a few kinematic observables which can be used, in addition to cuts C1-C6, to reduce the SM backgrounds. For example, we can optimise \( d_\perp \) for both the leading two leptons, especially the second lepton which, for signal events, has larger \( p_T \) and longer decay lengths (see plots in the upper panel of figure 6). Another important quantity is the ratio of the missing transverse momentum and scalar \( H_T \), defined as \( \alpha = \frac{p_T}{\sqrt{H_T}} \). Signal events have large missing transverse energy and, therefore, relatively larger values of \( \alpha \). These additional observables provide us with an extra handle to minimise the SM backgrounds and improve the sensitivity to sneutrino events.

### 5 Extraction of Yukawa couplings

In order to extract the Yukawa couplings, we need to know the spectrum. The heavy Higgs masses can be measured reasonably accurately from their fermionic decay channels. The higgsinos would also be discovered from other searches and those would give an estimate for the masses of the neutralinos and charginos. The sneutrino mass can be estimated by measuring the invariant mass of the DV related to the sneutrino decay to a lepton and a chargino. The invariant mass distribution has an endpoint at \( m_{\tilde{N}} - m_{\tilde{\chi}^\pm} \) (see figure 5), which will give us the sneutrino mass once we know the chargino mass.

| Cut | BP-I | BP-II | BP-III | \( tt \) | \( b\bar{b} \) (30 GeV) | \( b\bar{b} \) (200 GeV) |
|-----|------|-------|--------|-------|----------------|----------------|
| C1  | 420.4| 354.9 | 160.6  | 2637.8| \( 2.7 \times 10^7 \) | 440.2         |
| C2  | 354.7| 335.8 | 71.9   | 857.0 | \( 2.4 \times 10^6 \) | 362.5         |
| C3  | 315.3| 309.1 | 57.6   | 384.9 | \( 1.2 \times 10^6 \) | 176.1         |
| C4  | 314.7| 307.8 | 56.9   | 384.9 | \( 1.2 \times 10^6 \) | 176.1         |
| C5  | 314.7| 307.3 | 56.9   | 384.9 | \( 1.2 \times 10^6 \) | 176.1         |
| C6  | 265.8| 270.4 | 49.6   | 123.2 | 32432.1        | 150.2         |
| C7  | 35.9 | 1.7   | 13.5   | 5.1   | 0              | 5.2           |

Table 3. Cutflow table (\( \sqrt{s} = 13 \) TeV and \( \mathcal{L} = 137 \) fb\(^{-1} \)).

|      | Signal (S) | B (\( tt \)) | B (\( b\bar{b} \)) | B (total) | Significance = \( \frac{S}{\sqrt{S+B}} \) |
|------|------------|--------------|---------------------|-----------|---------------------------------|
| BP-I | 35.9       | 5.1          | 5.2                 | 10.3      | 5.3                             |
| BP-II| 1.7        | 5.1          | 5.2                 | 10.3      | 0.5                             |
| BP-III| 13.5      | 5.1          | 5.2                 | 10.3      | 2.8                             |

Table 4. Signal significances estimated at \( \sqrt{s} = 13 \) TeV and \( \mathcal{L} = 137 \) fb\(^{-1} \).
We assume that we are able to get an essentially background free sample (say, over 95% purity) using the cuts given in the previous section (both those given in table 3 and discussed at the end of the section) and the usage of $b$-tagging. We then do an event-by-event correction to the displacements described in section 3 to get the actual lifetimes. As both the CP-even and CP-odd Higgs bosons contribute to the signature, we need to pick which mass we use in the boost correction. As discussed in [21], the CP-even Higgs state usually has the largest BR to sneutrinos, although also the amount of available phase space has an impact. If the CP properties of the two heavy Higgses have been measured, the CP-even mass would give the better estimate, otherwise it would be a reasonable choice to pick the heavier one due to the larger phase space. This ambiguity leads to a systematic error in the measurement of the Yukawa couplings, which is of the order of 10% estimated by studying the impact of choosing the other Higgs mass to the lifetime distribution.

The background originating from heavy flavour hadrons that survives the cuts is heavily boosted (with the $p_T$ of a typical $b$-jet being 200 GeV or more) leading to an average displacement greater than 5 mm. As the boost correction assumes the particle to be heavy, the lifetime of heavy flavour hadrons will be overestimated and will on average correspond to mean decay lengths around 5 mm, although the exponential distribution of course gives events at all displacements. We shall use a binning of 0.1 mm. As the total number of background events at the HL-LHC is expected to be around 200 (scaled from table 4 to
Figure 7. The fit of an exponential to the lifetime distribution of the sneutrino for BP-I. The amount of data corresponds to $3000 \text{ fb}^{-1}$ at $\sqrt{s} = 14 \text{ TeV}$.

$3000 \text{ fb}^{-1}$) and these are distributed into some 100 bins or more, there will not be many background events in a single bin. The background distribution may be estimated, e.g., by looking at events with small vertex mass and $p_T/\sqrt{H_T}$ and subtract it from the distribution.

The signal region includes a cut on the transverse distance of the leptons requiring $d_{\perp} > 0.2 \text{ mm}$. The distribution of lifetimes close to the cut will be modified and hence we put a lower bound on the lifetime when fitting. We fit the exponential to the distribution in the interval $0.5 \text{ mm} < c\tau < 5 \text{ mm}$. This leads to rather robust results if the true lifetime is around $c\tau \approx 1 \text{ mm}$ but, if the lifetime is shorter, the number of events in the fit region becomes so low that the statistical error increases. In such a case it might be reasonable just to use this method to find an upper limit for the lifetime and derive a lower limit for the neutrino Yukawa couplings. An upper limit for the Yukawa couplings can be obtained from the constraint on the sum of neutrino masses. That can be expressed as

$$\sum m_\nu = \text{Tr}(m^\nu) = \sum_{i,j} |y^\nu_{ij}|^2 v^2 \sin^2 \beta/2m_{N_j}.$$  

Once we had studied the fitting method with one BP, we tried to analyse other BPs blindly so that one of the authors generated events and another one then analysed them, the result was then compared to the unknown input. As long as the decay lengths were at the mm scale, a reasonable agreement was achieved. We show in figure 7 a fit of the sneutrino lifetime for BP-I. We fit a simple exponential to the lifetime distribution. The fit with a number of events corresponding to HL-LHC energy ($\sqrt{s} = 14 \text{ TeV}$) and luminosity ($3000 \text{ fb}^{-1}$) gives us $\sum |y^\nu_{11}|^2 = (2.62 \pm 0.13 \pm 0.26) \times 10^{-13}$, where the first error is statistical and the second one the theory error (assumed to be 10%) from the ambiguity in choosing the CP-even or CP-odd Higgs as discussed above. On top of these there will be experimental systematic errors, which are mostly related to measuring the primary and secondary vertices. The true value is $2.28 \times 10^{-13}$, which is slightly more than one standard deviation off. For BP-II the event sample is so small that the Yukawa couplings cannot be reliably estimated. The best fit value would have been $3.57 \times 10^{-13}$ but, as the actual average decay length is shorter than the lower end of our fitting region,  

\footnote{As this is a simple lifetime measurement, many typical sources for systematic errors, like parton distribution functions, do not matter.}
this estimate is based only on few events and individual outliers can significantly change the result. The estimate was off by a factor of two. With such a short decay length it makes sense only to give a lower bound on the Yukawa couplings. We give the results for our three BPs in table 5. When doing the estimate, we added 10% to the invisible decay width of Equation (3.4) due to the mixing effect of LH and RH neutrinos (see footnote on page 4).

From this value we can then determine the absolute values of individual Yukawa couplings as the number of events with a given lepton flavour, which will be proportional to $\epsilon_i |y^\nu_i|^2$, where $\epsilon_i$ is the efficiency of identifying the lepton of flavour $i$. Since the error on $|y^\nu|^2$ will often be below 20% with high enough statistics, the error on the Yukawa couplings themselves will be around 10%. Hence even this rather simple fitting method can give a reasonably good estimate of the Yukawa couplings.

### Table 5

|                | BP-I            | BP-II           | BP-III          |
|----------------|-----------------|-----------------|-----------------|
| Measured $\sum |y^\nu_i|^2$  | 2.62 $\pm$ 0.13 $\pm$ 0.26 | $> 2.94$         | 3.73 $\pm$ 0.67 $\pm$ 0.37 |
| Actual $\sum |y'^\nu_i|^2$ | 2.28            | 7.81            | 2.40            |

The sums of neutrino Yukawa couplings from displacements and the actual input values in units of $10^{-13}$. The first uncertainty is statistical and the second one is a 10% theoretical uncertainty related to the ambiguity between the CP-even/odd Higgs states as discussed in the text. For BP-II the decay length was so short that we only quote a lower limit for the Yukawa couplings.

### 6 Conclusions and outlook

We have studied sneutrino pair production via the heavy Higgs portal in the NMSSM with RH neutrinos. In the model both higgsinos and RH neutrinos get their masses through the singlet VEV, so we expect them to be at the EW scale. If RH sneutrinos are heavier than higgsinos, they can decay to both a charged lepton and a chargino or a neutrino and a neutralino, the former one giving a visible signature at colliders.

Since the RH sneutrinos are gauge singlets, their decay modes are dictated by the neutrino Yukawa couplings, which are tiny in an EW scale seesaw model. The smallness of the decay width together with the lepton number violation arising from the RH (s)neutrino mass term leads to a signature with same-sign dileptons emerging from displaced vertices together with missing transverse momentum. The SM backgrounds for such a signal topology are therefore low.

We have indeed performed an analysis proving that the study of the emerging signatures with DVs can lead to the extraction of the neutrino Yukawa couplings, which salient features are as follows.

- We searched for displaced leptons and jets, with the leptons originating from sneutrino decays. Several BPs of the aforementioned BSM scenarios were introduced, with varied displacement lengths, and studied by MC analysis assuming a simple cut-based analysis providing a good signal-to-backgroud ratio already at the end of the 13 TeV run of the LHC.
• The kinematic distribution of the displaced vertex mass gives an end point which can be used to estimate the sneutrino mass once the chargino mass is known.

• Additional variables can make the regions of phase-space effectively background-free, thereby implying better handle on the extraction of the intervening Yukawa couplings.

• The decay width of the RH sneutrinos are dictated by the sum of the squares of the Yukawa couplings so a measurement of the sneutrino lifetime would allow one to measure the Yukawa couplings. The individual Yukawa couplings can then be extracted from the sneutrino BRs to different lepton flavours, once corrected with identification efficiencies.

• We ultimately showed that, for lifetimes corresponding to mm scale displacements, lifetimes can be measured with reasonable accuracy, which can then give the absolute values of the Yukawa couplings with a 10% accuracy so long that sufficiently large data samples can be accrued for the signal, like, e.g., at the HL-LHC.

In short, such an approach can lead to the extraction of the underlying neutrino dynamics parameters from the study of sneutrinos signatures at hadronic colliders, albeit under a specific SUSY paradigm. The results obtained here from events with DVs therefore complement those obtained in refs. [21, 22] for the case of prompt signatures.

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