Slug flow as tool for selectivity control in the homogeneously catalysed solvent-free epoxidation of methyl oleate

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Abstract
Catalytic oxidation of sustainable raw materials like unsaturated fats and oils, or fatty acids and their esters, lead to biobased, high-value products. Starting from technical grade methyl oleate, hydrogen peroxide as a green oxidant produces only water as by-product. A commercially available, cheap water-soluble tungsten catalyst is combined with Aliquat® 336 as a phase-transfer agent in solvent-free reaction conditions. In this study, we first report the transfer of this well-known batch system into continuous mode. The space–time yield is improved from 0.08 kg/L.h in batch to 1.29 kg/L.h in flow mode. The improved mass transfer and reduced back mixing of the biphasic liquid–liquid slug flow allows for selectivity control depending on physical parameters of slug flow namely volumetric phase ratio, volumetric flow rate, and slug length. Even though the product, methyl 9,10-epoxystearate is obtained at a maximum selectivity of only 58% in flow mode, higher space time yield combined with possible reactant recycling in flow mode offers a promising avenue of research. This work analyses the use of slug flow parameters as tools for controlling selectivity towards oxidation products of methyl oleate.

Keywords
Phase transfer catalysis · Flow chemistry · Epoxidation · Peroxopolyoxotungstates · Slug flow

List of Symbol

| Symbol   | Definition                                      |
|----------|-------------------------------------------------|
| $D$ [m]  | Diameter                                        |
| $\Delta p$ [bar] | Pressure difference                          |
| $V$ [ml min$^{-1}$] | Volumetric flow rate                          |
| $\Delta H$ [kJ mol$^{-1}$] | Enthalpy of reaction                          |
| $L$ [mm] | Segment length                                  |
| $F_{org}/F_{aq}$ [-] | Volumetric flow rate (organic/aqueous) |
| RPM [min$^{-1}$] | Revolutions per minute                        |
| $S$ [-] | Selectivity                                     |
| $X$ [-] | Conversion                                      |
| UFA      | Unsaturated fatty acid                         |
| SFA      | Saturated fatty acid                            |
| FAME     | Fatty acid methyl ester                        |
| MO       | Methyl oleate (Oleic acid methyl ester)        |
| $H_2O_2$ | Hydrogen peroxide                               |
| TPA      | Tungstophosphoric acid                         |
| $C$      | Catalyst                                        |
| PTC      | Phase transfer catalyst                         |
| OA       | Oleic acid                                      |
| ESAME    | Methyl 9,10-epoxystearate                       |
| DSAME    | 9, 10-Dihydroxystearic acid methyl ester       |
| PA       | Pelargonic acid                                 |
| PR       | Phase ratio                                     |
| MMA      | Monomethyl azelate                              |
| Aliquat® 336 | Methyltriocyl ammonium chloride              |
| CPC      | Cetylpyridinium chloride                        |
| POM      | Polyoxometalate                                 |
| PPOM     | Peroxopolyoxometalate                           |
| QAS      | Quaternary ammonium salts                      |
| DoE      | Design of experiments                           |
| FCCC     | Face centred central composite design           |
| $T$ [°C] | Temperature                                     |
| TFR      | Total flow rate                                 |
| $SV$ [mm$^3$ s$^{-1}$] | Slug velocity |
| $SL$ [mm] | Slug length                                    |
| $U$ [mm s$^{-1}$] | Velocity                                      |
| $\eta$ [mPas] | Dynamic viscosity    |
| $D$ [mm] | Diameter                                        |

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SG Slug generator
Ca “[−]” Capillary number
h “[µm]” Wall film thickness
R “[m]” Radius
FS Flow sensors
FEP Fluorinated ethylene propylene
PTFE Polytetrafluoroethylene
PS Pressure sensors

Introduction

In terms of Green chemistry, fats and oils can serve as highly attractive substrates for the sustainable chemical industry [1]. Through selective epoxidation of the internal double bond of unsaturated fatty acids or derivatives, bio-based epoxy compounds can be formed [2]. As an example, epoxidized soybean oil is applied as a plasticizer and stabilizer for poly(vinyl chloride) [3]. Additionally, ring-opening oligomerization and reduction to primary alcohols can be applied for the synthesis of renewable resource-based polyurethanes [4]. Furthermore, epoxides can be used for coatings, paints, or lubricants [5]. A very environmentally benign epoxidation method includes the application of hydrogen peroxide, air, or even pure oxygen as green oxidants [6]. Due to their low molecular weight and the therefore high relative amount of active oxygen, a lower environmental factor relating to Sheldon’s definition of the mass of waste per mass of value product occurs [7] compared to toxic, inorganic oxidants such as CrO₃, KMnO₄ and MnO₂ [8]. On the other hand, the use of oxygen-rich oxidants often results in exothermic side-reactions that are hard to control, especially on an industrial scale. The Prileshajev epoxidation with organic percarboxylic acids, formed from H₂O₂ and a carboxylic acid, is commonly used, although extremely acidic conditions are caused by the application of formic or acetic acid as oxygen transfer agents and strong inorganic acids as catalysts. Consequently, corrosion might be an issue, and neutralization and separation of the acid are required before subsequent conversion of the product. Therefore, epoxidation routes based on transition metals or enzymes are highly favourable [9, 10]. The oxidant, hydrogen peroxide, is directly used without the formation of percarboxylic acids resulting in non-acidic, non-corrosive conditions. Generally, due to the low polarity of long-chained fatty acid methyl esters, epoxidation with aqueous hydrogen peroxide is challenging [11]. However, several transition metal catalysts based on e.g. Ru, Os, W, and others have been applied to epoxidation reactions of unsaturated fatty acids and their derivatives. Amongst them, tungsten is highly advantageous due to its cheaper price and lower toxicity. Especially tungsten polyoxometalates (POMs) such as Keggin-type heteropoly acid tungstophosphoric acid (H₃PW₁₂O₄₀-TPA) have been in the focus of research, usually applied in a two-phase system with a phase transfer agent (PTA) allowing for organic solvent-free reaction conditions as developed by Venturello [12]. Commonly used phase transfer agents are e.g. cetyl pyridinium chloride (CPC) and methyltrioctylammonium chloride (Aliquat® 336) [1]. Mechanistically, the oxygen atom is first transferred from hydrogen peroxide to the heteropolyanion. After the transfer of the peroxo POM through a PTA into the organic phase, the oxygen atom can be transferred to the substrate. The remaining POM is then regenerated by H₂O₂ at the interface [13] making mass transfer limited at the interface.

To improve mass transfer, the implementation of capillary microreactors can be considered. The small dimensions result in a high surface to volume ratio between the two liquids, causing external heat transfer and internal mass transfer. Moreover, superior reaction performances can be achieved in a continuous reactor that does not employ any mechanical moving parts to increase the contact between the biphasic medium.

The liquid–liquid slug flow is a two-phase flow regime that occurs in capillaries, offering several characteristics beneficial to the performance and controllability of two-phase reaction systems. It is made up of two immiscible liquids where one liquid shows a higher affinity toward the capillary material. The high-affinity liquid forms a continuous phase in which the other liquid is present in the form of disperse slugs, separated from the capillary by a thin wall film as illustrated in Fig. 1 [14].
The presence of the wall film has non-negligible effects on both pressure drop, as well as mass transfer between the two phases [15, 16]. Its width \( h \) in relation to the capillary radius \( R_c \) may be calculated using the capillary number \( Ca \) of the continuous phase [17]:

\[
h = 1.34R_cCa^{2/3}
\]  

(1)

\[
Ca = \frac{\eta s}{\sigma}
\]  

(2)

Another important characteristic of the liquid–liquid slug flow with importance toward mass transfer lies in the flow pattern within the slugs and inter-slug regions. Due to frictional forces and barriers posed by phase interfaces Taylor vortices may form. A quantitative analysis of the flow pattern with liquid–liquid slug flows (using a paraffin-water model system) by Kashid et al. employs the dimensionless recirculation time \( \tau \) as a measure of vortex intensity. [18]

\[
\tau = \frac{L_s (R^2 - R_0^2)}{2L_s \int R \ U(r) rdR}
\]  

(3)

Re-circulation time \( \tau \) (describing the number of times a slug travels its own length until a typical fluid element has moved from one side of the slug to the other) thus depends upon the slug length \( L_s \), slug velocity, radial velocity profile \( U(r) \), radial position of the vortex boundary \( R \) as well as the radial position of the vortex centre \( R_0 \). Using particle tracing techniques as well as CFD modelling, the study finds that circulation times for both aqueous, as well as for organic phase lie between 3 and 4 for systems exhibiting a wall film, changing only slightly with slug flow velocity and slug length at the flow rates considered in this work [18]. This means the vortex circulation velocity rises proportionally with the total flow rate. The presence of Taylor vortices is an advantage of the slug flow regime, positively impacting mass transfer by facilitating the internal mixing of the phases without the need for intrusive agitators [15]. Overall volumetric mass transfer coefficients of 0.88 – 1.67 s\(^{-1}\) are reported for slug flows in capillaries with inner diameter 0.5 – 1 mm, thus providing a favourable environment for two-phase reaction systems [14, 19]. Using the example of the nitration of aromatics in a slug flow reactor, Dummann et al. show that conversion and the formation of by-products can be influenced simply by altering the flow velocity [19]. Slug flows are further characterized by their slug length and phase ratio. The slug length is dependent on the geometry of the phase mixer (referred to as slug generator), while the phase ratio is dependent on the individual flow rates supplied to the slug generator [16, 20]. Due to the well-defined nature of the flow pattern, the slug length and phase ratios of slug flows are strongly related to the amount of available interfacial area [14]. By adjusting the slug length and the phase ratio, the performance of mass transfer limited two-phase reactions may be further impacted.

In addition to mass transfer limitation in biphasic reaction media resulting in limited conversion, selectivity must be considered due to side- and subsequent reactions in terms of sustainable process development. Regarding the epoxidation of methyl oleate using the described catalyst system [20–22], full oxidative cleavage towards aldehydes or carboxylic acids is likewise feasible (Fig. 2) [23, 24]. Although the latter valuable bio-based products are obtained on an industrial scale [25] and exhibit various applications, selectivity must be controlled.

Considering the above-mentioned characteristics, slug flow reactors pose a promising basis for process intensification. Processes like two-phase reactions, which usually depend on active agitation, considerable residence times, and subsequent phase separation can be achieved with
minimal moving parts (i.e. in-line phase mixing using the slug generator) and small volumes due to highly effective mass and heat transfer [14, 20]. Furthermore, by including a continuous separation device based on wetting behaviour as demonstrated by Gaakeer et al. and Scheiff et al., the slug-flow reactor could potentially deliver two separated process streams, achieving mixing, reaction and phase separation in a combined process [21, 22].

In the present work, the biphasic epoxidation of methyl oleate is transferred from batch to continuous liquid–liquid slug flow mode. TPA is solved in the aqueous hydrogen peroxide phase, whilst methyl oleate and the phase transfer agent form the organic phase. Special emphasis is on an improved mass transfer through control of physical parameters such as slug length, volumetric flow rate, and phase ratio which are also found to be tools to control selectivity.

**Batch Experiments & Results**

These experiments are performed with technical grade MO (Inkemia Green Chemicals) containing 70% MO by weight. The impurities consist of the saturated fatty acid methyl esters methyl palmitate and methyl stearate. 1.5 g (0.0035 mol) of technical grade MO is used for every experiment and 35% H₂O₂ (Carl Roth GmbH) is chosen for the experiments as highly concentrated H₂O₂ is potentially risky. Aliquat ® 336 (Alfa Aesar) and Tungstophosphoric acid (Carl Roth GmbH) constitute the remaining of the reaction mixture.

Batch experiments are performed for the epoxidation of MO with a phase transfer catalysed—catalytic system with H₂O₂ as the oxidant. Experiments are also performed on the epoxidation of methyl oleate with Tungstophosphoric acid (TPA) as the catalyst and Cetylpyridinium chloride (CPC) as the Phase Transfer Catalyst (PTC) to selectively produce methyl 9,10-epoxystearate. The low solubility of CPC in the reaction medium and the presence of solid after the reaction quenching makes CPC an undesirable candidate for continuous operations. Aliquat® 336 is reasonably soluble in water making it a candidate for continuous mode operation. Batch experiments with Aliquat® 336 as PTC are, hence, necessary, as these parameters from batch experiments are used as the basis for the continuous experiments. Further details pertaining the experimental procedure in batch mode can be found in Appendix A.

**Optimization of batch epoxidation of methyl oleate using Statistical design of experiments**

To achieve the high conversion of methyl oleate (MO) and selectivity of epoxide, the statistical design of experiments is employed. An experimental plan is created including the most relevant factors influencing the system, such as the molar ratio of oxidant to the substrate (H₂O₂/MO), the molar ratio of substrate to the catalyst (MO/C), the molar ratio of PTC/C, temperature, reaction duration and stirring speed [23, 24]. A statistical evaluation provides numerous advantages over manual evaluation when each factor is varied from one experiment to the next. Hence, the experiments are designed with the help of Modde 10.1 (More details in Appendix B).

Pai, Tolstikov et al. reported that, at lower temperatures/ambient temperatures, very low conversion of olefins and alcohols is achieved [24]. Godard, Caro et al. observed higher temperatures increasing the possibility of unwanted side reactions as well as the decomposition of H₂O₂ to water and oxygen [25]. Taking these effects into consideration the operating window of temperature is chosen as 50 to 80 °C.

Khlebnikova, Pai et al. proved that TPA forms tetra nuclear peroxopolyoxotungstate complex with H₂O₂ [23, 26]. Increasing the amount of catalyst therefore increases the amount of tetranuclear peroxopolyoxotungstate complex, resulting in increased reaction rates. Simple screening experiments are carried out to determine the operating window for the variable MO/C and is fixed from 50 to 200. The deciding factor in the lower limit of MO/C is the solubility of TPA in the organic phase. Since H₂O₂ is a mild oxidant, no reaction is observed with this Catalyst/PTA combination with MO/C greater than 200, hence the upper limit.

Theoretically, one molar equivalent of H₂O₂ is sufficient for epoxidation of the double bond in MO to form methyl 9,10-epoxystearate. Four molar equivalents of H₂O₂ reacting with one molar equivalent of MO results in oxidative cleavage of MO. Godard, Caro et al. have reported the requirement of a higher H₂O₂/MO molar ratio for oxidative cleavage due to the increased decomposition of H₂O₂ at higher reaction temperatures [25]. Since the selectivity of the epoxide is being considered, the bounds for the molar ratio of H₂O₂/MO are chosen as [1,4].

The organic and aqueous phases are immiscible, making the effect of stirring speed an important factor. At higher stirring speeds (more than 600 RPM), a decrease in the yield of the product is observed during the screening experiments. This could be attributed to the introduction of oxygen bubbles in the reaction medium, with these oxygen bubbles decreasing the contact between the substrate and oxidant in a sealed batch reactor. No significant conversion of MO occurred with stirring speeds lower than 100. Therefore, the stirring speed is varied between 100 to 600 RPM.

Pai, Tolstikov et al. believe that the peroxo anion \{PO₄\[WO(O₂)₂]₁₄\}⁻ is the active ionic species that transfer the oxygen to the organic phase due to the formation of a coordinate complex with a PTC in their system [24]. The amount of catalyst and PTC could therefore be inferred to have a direct impact on the conversion of MO and the selectivity of...
products. The molar ratio of PTC/C varies between 1 and 6. For ratios greater than 6, the selectivity of the product and conversion of MO are adversely affected. This is attributed by Pai, Tolstikov et al. to the lipophilicity of the participating cationic species of PTCs in the effective/ineffective transfer of peroxo-anion [24].

Khlebnikova, Pai et al. carried out such reactions for times varying from 1–5 h, and the same time frame is selected for these experiments [23]. The list of factors varied for the DoE is summarized in Table 1.

The conversion of MO and the selectivity of methyl 9,10-epoxystearate, are set as the optimisation variables. The minimum and maximum limit for the conversion is set at 50 and 100% respectively and for selectivity of epoxide as 30 and 100% respectively. The target value for this procedure is set as 90% and 70% respectively, based on the figures obtained in similar literature.

Karmoker, Hasan et al. have similar systems and reported good results using the RSM Optimisation technique (Response surface methodology—RSM) [27, 28]. The same is chosen as the objective for this optimisation. The number of experiments required for identifying optimal reaction parameters depends on the number of factors. The difference in the number of experiments between conventional design and an FCCC—it designed model is shown in Table 11 (Appendix C). The experiments are performed, and all the results are shown in Table 12 in Appendix D. For the model created using FCCC-design, the effect of factors on the conversion of MO, as determined by statistical analysis, is shown in Fig. 3. The green bars represent the effects of individual factors and interacting factors. The effects being positive or negatively affects the conversion, respectively. The error bars represent the magnitude of the effect by each factor, the variability of the data, and the uncertainty in a reported measurement graphically. If the error bar includes zero, the factor becomes insignificant.

Figure 3 shows that the molar ratios of PTC/C, H$_2$O$_2$/MO, stirrer speed, and reaction time have a positive linear influence on the conversion of MO. The negative quadratic influences should be neglected since the error bars include the zero line. The stirring speed has the largest influence on conversion. The stirring of the reaction system increases the contact between the organic and aqueous immiscible phases by increasing the surface area of contact due to the turbulence. The increase in turbulence results in increased surface area available for the reactants to interact with the oxidant/peroxo-anion, resulting in higher conversion. Furthermore, the large impact of stirring speed on conversion implies that the overall reaction system is limited by mass transfer in the range of stirring speeds used in this work.

The higher molar ratio of H$_2$O$_2$/MO implies increased production of oxidants. High PTC/C ratios result in increased transportation of active ionic species from the aqueous phase to the organic phase, thereby increasing the amount of active peroxygen in the organic phase giving higher values of conversion. The molar ratio of MO/C and temperature does not have any linear or quadratic influence on the conversion of MO. However, some combination of these factors does influence the system. For example, there is a strong positive interaction between MO/C molar ratio

| Table 1 List of factors and their ranges for DoE |
| Factors | Limits |
| Temperature (°C) | 50–80 |
| PTC/C (molar ratio) | 1–6 |
| MO/C (molar ratio) | 50–200 |
| H$_2$O$_2$/MO (molar ratio) | 1–4 |
| Stirrer speed (rpm) | 100–600 |
| Time (hours) | 1–5 |

Fig. 3 Influence of the factors on the conversion of methyl oleate, where Temp – Temperature, PTC:C – n$_{PTC}$/n$_C$, MO:C – n$_{MO}$/n$_C$, H$_2$O$_2$ – n$_{H2O2}$/n$_{MO}$ & Sti – Stirrer speed
and stirrer speed as well as $H_2O_2/MO$ molar ratio and stirrer speed and a negative interaction for PTC/C and MO/C.

The effects of factors on the selectivity of epoxide are shown in Fig. 4. Contrary to what is shown in Fig. 3, the effect of temperature and the molar ratio of MO/C has a positive linear influence on the selectivity of epoxide in comparison to conversion. The strong positive influence of MO/C can be explained by the fact that the increase in MO/C results in a decrease in the amount of catalyst in the reaction system. The lower amount of catalyst consequently reduces the amount of peroxy-anion formation, thereby reducing the further oxidation of MO into consecutive products resulting in the selective production of methyl 9,10-epoxystearate. Time has a strong negative linear influence on the selective production of the epoxide. With the increase in reaction time, the oxidation of MO can proceed to the next steps, resulting in lower yields of the epoxide.

Temperature notably influences the selective production of methyl 9,10-epoxystearate. Higher reaction medium temperatures lead to an increase in the decomposition of $H_2O_2$, leading to higher concentrations of oxygen radicals, which in turn lead to the formation of oxygen gas, limiting the number of oxidizing radicals available for oxidizing MO to further products. Although $H_2O_2/MO$ does not have any linear significant impact on selective epoxidation, it should still be considered since it has a significant effect while combined with other factors. The interaction factor of MO/C and $H_2O_2/MO$ also influences the reaction system. Without the linear effects, no quadratic and interacting effects are included in the model. Contour plots of both system responses (conversion and selectivity) are shown in Figures 20 and 21 in Appendix D.

The optimized reaction conditions are shown in Table 2 and the predicted conversion of MO and selectivity of methyl 9,10-epoxystearate at those conditions are shown in Table 3. Table 3 shows that the experimentally obtained results are within a 10% margin of the predicted results. Figure 5 shows the deviation of all experimental results from the DoE-model (Coefficients listed in Tables 13 and 14 in Appendix D). The obtained values are in no way comparable to the results obtained by Kozhevnikov, Mulder et al. [11], reaching 95% conversion with 89% selectivity towards epoxide. However, the main objective of this work is not optimising conversion and selectivity in batch mode or for that matter in flow mode, but to determine the possibility of selectivity and product control in a flow reactor using slug flow parameters. Also, compared to Kozhevnikov, Mulder et al., this work employs relatively simple and cheap catalyst and PTC. The optimal parameters obtained in the batch mode are taken as the source for calculating the material

### Table 2 Parameters optimized for Epoxidation in a Batch reactor

| Factors                | Optimal values |
|------------------------|----------------|
| $H_2O_2/\text{MO}$ (molar ratio) | 1.13           |
| MO/C (molar ratio)     | 194            |
| PTC/C (molar ratio)    | 5.7            |
| Temperature            | 60 °C          |
| Stirrer speed          | 500 rpm        |
| Duration of the reaction | 2.7 h         |

### Table 3 Predicted results by the DoE vs Experimental results

|                        | Predicted value | Experimental value |
|------------------------|-----------------|--------------------|
| Conversion of MO       | 80%             | 73%                |
| Selectivity of Epoxide | 55%             | 52%                |
quantities necessary to perform epoxidation of MO in continuous flow mode.

Flow Experiments & Results

A flow diagram of the experimental plant used in this work is shown in Fig. 6. The experimental slug flow reactor consists of a capillary made from fluorinated ethylene propylene (FEP) with a total length of 15 m and an inner diameter of one millimetre with three equidistantly spaced sampling ports located along the length of the reactor. Methyl oleate and PTC form the continuous phase while the disperse phase slugs are made up of the aqueous Hydrogen peroxide/TPA solution. Both phases are supplied using micro annular gear pumps (HNP microsystems GmbH, mzr-2921), and their flow rates are monitored by micro-scale flow sensors (Sensirion AG, Liquid Flow Meter SLI). The individual flow rates are controlled by pump rotations per minute (RPM).

Pressures of the supply channels as well as at the reactor outlet are measured by pressure transducers (Afriso-Euro-Index DMU-03).

Arsenjuk et al. and Vietinghoff et al. developed systems where the slug length at the reactor inlet is measured by an optical sensor shown in Fig. 7 consisting of a double infrared gate, where the passage of aqueous slugs through the infrared beam results in a reduction in measured beam intensity [29, 30]. The slug flow is formed in the slug generator shown in Fig. 8 – developed by Arsenjuk et al. – which features an adjustable geometry, allowing for the slug length in the slug flow reactor to be controlled [20]. The reactor is placed in a water bath heated to 60 °C. Due to the small volume and high specific area of the capillary, isothermal reaction conditions may be assumed [19]. At the reactor outlet, a needle valve (Swagelok SS-SS1-A) is placed and connected to a stepper motor to control pressure.

Data is gathered from the sensors using an analogue data acquisition device (National Instruments NI-9205) and
processed using a program written in LabVIEW, a graphical programming environment executed on a computer. Control outputs to the pumps are issued by an analogue data output device (National Instruments NI-9264) while the stepper motors positioning slug generator and needle valve are controlled by a driver board (Trinamic TMCM-610) which receive instructions from the computer. This automated setup with a continuous flow microcapillary reactor allows the impact study of these parameters on reaction conversion and selectivity.

Gemoets, Su et al. state that the overall performance of an oxidation reaction is mainly determined by intrinsic kinetics and transport properties inside the reactor. They also make a case that for a fast liquid-phase oxidation reaction, the reaction rate and selectivity are influenced by the mass transfer rate and internal circulations within the slugs along with reaction kinetics [30]. The individual effects of the setpoints, i.e., volumetric flow rate, phase ratio, and the length of the slugs, on the solvent-free Aliquat® 336 assisted oxidation of MO are discussed in the following sections.

In the transition of parameters from batch operation to continuous operation, some of the terms must be adapted for their usage. This transition is explained briefly in the Appendix E. The chemicals used in the flow experiments are the same as the ones used in batch mode. The calculated space–time yield for the best yield of epoxide in Batch mode is 0.08 kg/L.h, whereas the best yields seen generally in flow reactors are usually in the range of 1–10 kg/L.h. The following results also demonstrate similar trends. The best space–time yields achieved in flow mode is 4.49 kg/L.h. The increased space–time yield for this reaction system is one clear reason to explore this reaction in the flow mode. Effects of various parameters in flow mode and the ability to control the reaction parameters are also studied in the following sections.

**Flow Results—Effect of length of flow reactor**

Flow results are represented along the length of the reactor. Results show that the conversion of MO always increases with the length of the reactor and in some cases plateaus after a certain amount of time spent in the reactor. This is true for most irreversible reaction systems. Due to the presence of various possible subsequent reaction paths, the general trend for the selectivity of MO towards epoxide is to decrease along the length of the reactor. However, both in the case of conversion and selectivity, the slopes of the curves have been proven to be controllable by controlling the respective slug flow variables.

Residence times, volumetric flow rates, and reactor length may at first glance seem like a set of redundant variables. However, that is not the case. Fixing a certain residence time by manipulating the reactor length and volumetric flow rate may theoretically constitute the same system. For example, a residence time of 10 min in a capillary microreactor could be achieved in any number of ways, 2 of which being, a reactor length of 10 m and a flow velocity (derived from volumetric flow rate) of 1 m/min and a reactor length of 20 m and a flow velocity of 2 m/min. However, recalling the dependence of recirculation time on slug velocity it is seen that the mixing characteristics of the system, like the stirring speed of
a batch reactor, is another control variable that affects the system in a non-trivial way [16, 18]. Thus, these variables are treated independently in this work and their individual effects are studied in a more detailed fashion.

Using the same catalytic system consisting of TPA and Aliquat 336® as used in this work, Wang et al. find that a simplified first-order kinetic model is sufficient to describe the epoxidation of 1,7-Octadiene with H2O2. Therein the complex of peroxo-anion {PO4 [WO(O2)2]4}3− and quaternary ammonium salt Aliquat 336® is assumed to be the active species. Assuming the concentration of active species \( c_{\text{cat}} \) in the organic phase is at pseudo-steady-state and that the reoxidation of the active species takes place in a boundary layer at the phase transition, they derive for the first epoxidation step of reactant A (with concentration \( c_A \)) in the organic phase: [31]

\[
\frac{dc_A}{dt} = -kc_{\text{cat}}c_A = -k_{\text{app}}c_A
\]  

(4)

where \( k \) is the intrinsic rate constant of the reaction and \( k_{\text{app}} \) the apparent rate constant. Integrating and adapting the above Eq. (4) to the system at hand yields:

\[
1 - \frac{c_{\text{MO}}}{c_{\text{MO,0}}} = X_{\text{MO}}(t) = 1 - \exp(-k_{\text{app}}t)
\]

(5)

The rate of reaction thus depends upon the (unknown) local concentration of the active catalyst species, which in turn depends on influencing factors, such as the goodness of mixing. In a subsequent publication, Wang et al. proceed to assess the influence of reaction conditions (stirring speed, reactant concentrations, etc.) on the overall reaction performance using the apparent rate constant. Therefore, in this work an apparent rate constant \( k_{\text{app}} \) is determined for different settings of the slug flow reactor and employed as a relative measure of reactor performance. Because only few points are available, the apparent rate constant is approximated by the slope-of-the-line method using the rearranged rate law (6) and linear regression of the data points. [31, 32]

\[
-\ln\left\{1 - X_{\text{MO}}(t)\right\} = k_{\text{app}}t
\]

(6)

Flow Results—Effect of Volumetric flowrate

Six Experiments are conducted to determine the effect of varying volumetric flow rates on the oxidation of MO. Two flow rates (0.8 ml/min and 1.6 ml/min) are analysed with two constant slug length and phase ratio combinations (PR 3 & SL 2 mm, PR 7 & SL 8 mm). The high conversions (greater than 95%) reached at longer reactor lengths (15 m) in almost all cases are to be noted. Since the work is done with microcapillaries, the effective reactor volume is also small (11.5 ml). This along with low residence times of 2 to 14.7 min, results in high space–time yields for epoxide in flow mode (4.49 kg/L h). Considering a measured power consumption of the stirrer of 3.8 W and a measured power consumption of the micro gear pumps of 5.9 W (combined), one mole of desired product (epoxide) under best observed reaction conditions requires 420.5 kJ/mol of mechanical energy in the slug flow reactor and 20,310.4 kJ/mol of mechanical energy in batch mode. Much of this is likely attributable to mechanical losses. Nonetheless, the mechanical power required by the slug flow reactor is substantially lower.

Naturally, because of the difference in residence time, the higher the volumetric flow rate the longer a reactor is

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**Fig. 9** Length vs Conversion & Selectivity plot with trend for variation in volumetric flowrate. Phase ratio – 3 (Forg/Faq); Slug length – 2 mm; Total Volumetric flowrate a) 0.8 ml/min [organic phase – 0.6 ml/min; aqueous phase – 0.2 ml/min] b) 1.6 ml/min [organic phase – 1.2 ml/min; aqueous phase – 0.4 ml/min]

**Fig. 10** Rearranged rate law vs residence time with line fit, Phase Ratio – 3, Slug length – 2 mm, for different total flow rates
required to achieve the same conversion levels. For example, in Fig. 9, for a phase ratio of 3 (Forg/Faq = 3) and slug length of 2 mm, the total volumetric flow rates are varied between 0.8 ml/min and 1.6 ml/min, leading to differing final conversions. In addition, the reactor length vs conversion curve shows that, at a total volumetric flow rate of 1.6 ml/min, the length of the reactor to achieve a conversion of 70% is ~8 m, whereas for a length of 4 m (i.e. constant residence time) 62% conversion of MO is achieved for a flow rate of 0.8 ml/min, indicating a faster progression of the reaction. This is further shown by Fig. 10 and the apparent reaction rate constants in Table 4. The reaction converting MO is slightly faster for a higher flow rate. This can likely be attributed to more intense mixing as the vortex intensity increases with slug velocity, which is proportional to the total flow rate.

In, the average selectivity of epoxide is 35.6% for a volumetric flow rate of 1.6 ml/min whereas the average selectivity is 27.6% for a volumetric flow rate of 0.8 ml/min. In this case, the flow rate has no discernible impact on the selectivity as both trend curves show roughly the same slope. The difference in average selectivity is likely due to the longer residence time. As MO depletes along the reactor, epoxide is converted to subsequent products while the production of epoxide slows.

As shown in Fig. 11, for a phase ratio of 7 and slug length of 2 mm, conversions for a 0.8 ml/min flow rate range from 50% at 4 m to 87% at 15 m of reactor length. The same for 1.6 ml/min range from 70 to 92%, showing similar trends as in the previous cases, however the reaction is over twice as fast for the higher flow rate in this case, marking a much greater increase (Fig. 12 and Table 5). The selectivity of epoxide is similar in this case for both the flowrates for most of the reactor length, with the selectivity for the higher flow rate being slightly slower. This could be attributed to the increased concentration of epoxide as well as to factors discussed in the section explaining the effect of phase ratio and slug length.

The contradicting forces at play can be seen as a means of controlling the reaction outcome within the context of the automated slug-flow control setup. It is shown that the same system with the same concentration of reactants can be manipulated physically, by controlling the slug flow parameters, to react differently enabling the possibility to exert a high degree of control on the system.

### Table 4
Apparent rate constants of MO epoxidation determined from Fig. 10 and average observed selectivity for different total flow rates. Phase ratio 3, slug length 2 mm

| Total Flow Rate in ml min⁻¹ | k_app in min⁻¹ | Average Selectivity Epoxide in % |
|-----------------------------|---------------|----------------------------------|
| 0.8                         | 0.174         | 27.6                             |
| 1.6                         | 0.229         | 35.6                             |

### Table 5
Apparent rate constants of MO epoxidation determined from Fig. 12 and average observed selectivity for different total flow rates. Phase ratio 7, slug length 2 mm

| Total Flow Rate in ml min⁻¹ | k_app in min⁻¹ | Average Selectivity Epoxide in % |
|-----------------------------|---------------|----------------------------------|
| 0.8                         | 0.179         | 34.0                             |
| 1.6                         | 0.381         | 28.8                             |

**Fig. 12** Rearranged rate law vs residence time with line fit, Phase Ratio – 7, Slug length – 2 mm, for different total flow rates.
as highlighted in Fig. 13, where various instances of a unit length microcapillary reactor are shown. An analogy to a batch reactor is drawn to clarify what is happening in this system.

Phase ratio being constant across a unit length of a microreactor is assumed to be equivalent to a fixed reactant concentration system in batch and a phase ratio change is analogous to changing the molar concentration in a batch reactor. Batch mode experiments with a fixed concentration of the reactants and different stirrer speeds are assumed to be analogous to case a) and case d) in Fig. 13. Similarly case b) and case c) also have the same concentration of reactants (phase ratio), but different interfacial areas.

Contrary to a batch reactor, where stirrer speed is the only control variable to affect physical mixing, in the flow mode, both volumetric flow rate (stirrer speed) as well as slug length (interfacial area) can be controlled. Temperature and other physical parameters do have a small effect on mixing, albeit these other effects affect both modes similarly. This extended degree of control allows this microcapillary system to not only have the advantages of a general flow reactor (reduced residence times & continuity in the system), rather also the ability to extract different conversions and selectivities with a fixed reactant concentration upstream the pumps.

Given the definition of the phase ratio \( PR \) according to formula (7), the volume-specific interfacial area available for mass transfer inside the slug flow reactor is proportional to the sum of the areas of all slugs \( A_{\text{Slug, tot}} \), which may be calculated from the volume of the reactor \( V_{\text{Reactor}} \) and the inner diameter of the reactor \( D_{\text{Reactor}} \) using formula (8). Assuming the width of the wall film \( h \) is very small compared to the capillary diameter and the side of the slugs do not offer surface area for mass transfer, formula (8) may be simplified to yield formula (9). Using the simplified formula it can be estimated that the specific area available for mass transfer lies between 36 – 250 m\(^2\)/m\(^3\), depending on slug length and phase ratio setting. If the side walls of the slugs take part in mass transfer the specific area increases by an order of magnitude, potentially improving mass transfer, but greatly reducing the relative impact of the slug length and phase ratio settings.

\[
PR = \frac{\dot{V}_{\text{org}}}{\dot{V}_{\text{aq}}} \quad (7)
\]

\[
A_{\text{Slug, tot}} = \frac{V_{\text{Reactor}} \pi (D_{\text{Reactor}} - 2h)^2 + 2(D_{\text{Reactor}} - 2h)L_s}{(1 + PR)^2 (D_{\text{Reactor}} - 2h)^2 L_s} \quad (8)
\]

\[
A_{\text{Slug, tot}} \approx \frac{2V_{\text{Reactor}}}{(1 + PR)L_s} \quad (9)
\]

For the sake of this particular explanation, volumetric flow is assumed to be constant across all cases. In the case of fixed phase ratio and increasing slug lengths, Case a) and d), as shown in Fig. 13, the amount of internal circulation in both the organic and the aqueous slugs decrease [16]. While the effect is comparatively small, according to Kashid et al., its presence and effect in mass transfer should not be neglected [18]. More importantly, the change in slug length means a change in the interfacial area \( A_{\text{Slug, tot}} \) according to Eq. (8). Overall, changes in slug length have several effects which may interplay, as convective transport within the slugs and interslug regions aids in reducing product accumulation at the interfaces while also facilitating transport of the active species to complete the catalytic cycle.

A way to exert a degree of control over the relative change in surface area is to use phase ratio as a control variable.
Considering the pairs, Case a) & b) and Case c) & d), where the slug lengths remain constant whilst the phase ratios change, it is clear that the internal circulation in the aqueous slug remains constant while the internal circulation in the organic interslug changes because of the increased volume. This, again, affects the local concentration of species reactants/products available for the reaction within the interslug regions. In the interslug regions in particular, more intense circulation may aid in the dilution of epoxide at the interface, preventing further reaction toward the diol product, thus improving selectivity. Because in this study an excess of hydrogen peroxide is present in all cases, the change in phase ratio is assumed to not affect the maximum attainable conversion. In Sect. 3.3.1 & 3.3.2, the effects of slug length and phase ratios are discussed from the results obtained in the respective flow experiments.

Effect of change in Slug length

Wada, Schmidt et al. [33] reported that the change in the size of the disperse phase slug affects the size of the continuous phase inter-slugs, i.e., phase ratio, in the context of Ozonolysis in a gas–liquid multichannel microreactor. However, in this work, owing to the design of the slug generator, the length of the aqueous slug is altered without having any effects on the phase ratio. Several experiments are hence conducted to understand the effect of change in slug lengths for a constant phase ratio since the effect of this characteristic has not been reported often before in literature.

Experiments are performed at different slug lengths (long and short slug lengths – 2 mm and 8 mm) and the results are recorded and discussed. The volumetric phase ratio and total volumetric flow rate are maintained at a constant value. Figure 14 shows the conversion/selectivity vs length plot for a reaction system with phase ratio 3, the volumetric flow rate of 0.8 ml/min, and different slug lengths of 2 mm and 8 mm. A higher selectivity of epoxide is observed for 2 mm slug length in comparison to slug length of 8 mm. It shows that a selectivity of 40% of epoxide is achieved at a reactor length of 4 m for a 2 mm slug length and the percentage of selectivity decreases along the length of the reactor. Lower selectivity of epoxide is reported for slug size of 8 mm in comparison to 2 mm slugs. Figure 15 shows similar effects of slug length on conversion for a different phase ratio of 7 and a volumetric flow rate of 0.8 ml/min. Selectivities along the reactor are nearly identical for both slug lengths at this setting, indicating that the increase in phase ratio may render any effects of changes in slug length insignificant (Tables 6 and 7).

Figure 13 and the subsequent description explains the possible impacts of slug length on the reaction. The increased internal circulation facilitates the mass transfer across the film, resulting in a higher, faster conversion of MO. However, since the change in slug length only affects mixing within the aqueous slug, it likely does not affect the subsequent reactions of epoxide disproportionately, meaning selectivity is not impacted significantly. This trend can also be observed in systems, where the increased inter-slug and slug sizes lead to increased conversion of MO.

Figure 15 also illustrate that a larger aqueous slug, which acts as a reservoir of H₂O₂ molecules, combined with the

| Slug length in mm | k_{app} in min⁻¹ | Average Selectivity Epoxide in % |
|------------------|------------------|---------------------------------|
| 2                | 0.174            | 27.6                            |
| 8                | 0.181            | 26.3                            |
controlled mass transfer of the oxidant to the organic phase with the help of catalyst and the PTC, shows an effect similar to continuous addition in the batch system.

On the contrary, Fig. 16 shows that for a higher total flow rate, slug length is much more important for both conversion as well as selectivity, with a larger slug length yielding a much higher reaction rate and lower selectivity. As discussed previously, an increase in flow rate increases the overall reaction rate for both slug lengths. In contrast with the expectation to see higher reaction rates with an increase in specific area, the addition of surface area leads to a worse result (Table 8).

As Ufer et al. show using various imaging methods, the initially assumed, ideal mixing behaviour may not hold up in all cases. Considering these observations (illustrated in Fig. 17), it becomes apparent that changing of the slug lengths may affect reaction outcomes in non-trivial ways [15]. This could explain why the change in reaction rate is very small for a small flow rate, despite a much larger specific area of the system at shorter slug lengths, as parts of the interfacial area are close to stagnant zones within the slugs, not benefitting from the good mass transfer implications of the Taylor vortices as shown in Fig. 17. It is also possible that more of the wall film than initially assumed takes part in the mass transfer. This implies that the interfacial area changes relatively little with slug length as described above. Because the wall film thickness increases with the slug velocity, some of the rate increase upon increase of the flow rate may in fact stem from an increased participation of the wall film in mass transfer.

**Effect of change in Phase Ratio**

In this case, the volumetric phase ratio of the system is changed by keeping the slug length and total volumetric flow rate at a constant value. The advantage of this system is its ability to manipulate the number of MO and $\text{H}_2\text{O}_2$ molecules available for the reaction system, as explained in Fig. 13. Compared to the batch mode, where further products are obtained due to the continuous addition of $\text{H}_2\text{O}_2$ [24], an easier solution is found in the continuous system.

In Figs. 18 and 19, for a fixed flow rate of 0.8 ml/min and a slug length of 2 mm and 8 mm, two-phase ratios are analysed. As can be seen from both the figures, smaller phase ratios, result in better conversion. Low phase ratios and small slugs, implies higher internal circulation, facilitating the transfer of peroxy anions ions to the interface. The reaction takes place in the organic phase and the transfer of peroxy anions is facilitated by the presence of quaternary ammonium cations in the PTC present in the organic phase. Since the number of moles of MO present for a phase ratio of 3 is less, the oxidation occurs early, and a higher conversion level is achieved at a relatively lower length. For a phase ratio of 7, the number of moles of MO to be oxidised is more. Therefore, the length of the reactor to achieve a certain value of conversion for a phase ratio of 7 is greater than for a phase ratio of 3 (Tables 9 and 10).

When the overall continuous reactor is considered, if the throughput of the reactor is considered, higher phase ratios in this case, actually mean a larger number of MO molecules taking part in the reaction. The availability of $\text{H}_2\text{O}_2$ molecules to the reaction system can also be controlled by this variable.

Table 7: Apparent rate constants of MO epoxidation and average observed selectivity for different total flow rates. Total flow rate 0.8 ml/min, phase ratio 7

| Slug length in mm | $k_{app}$ in min$^{-1}$ | Average Selectivity Epoxide in % |
|------------------|-------------------------|---------------------------------|
| 2                | 0.175                   | 34.0                            |
| 8                | 0.179                   | 33.4                            |

Table 8: Apparent rate constants of MO epoxidation and average observed selectivity for different total flow rates. Total flow rate 1.6 ml/min, phase ratio 3

| Slug length in mm | $k_{app}$ in min$^{-1}$ | Average Selectivity Epoxide in % |
|------------------|-------------------------|---------------------------------|
| 2                | 0.229                   | 35.6                            |
| 8                | 0.527                   | 18.9                            |

**Conclusion**

The work aimed to develop a homogeneous catalytic system to achieve high conversion of MO and selectivity of epoxide in biphasic flow mode and explore the possibility of using
slug flow variables to control reaction parameters, keeping the reactant feed streams’ concentrations constant. The catalytic system of $\text{H}_2\text{O}_2/\text{TPA}/\text{Aliquat}®$ 336 is employed for the oxidation of MO. Compared to Phimsen, Yamada et al., higher values of conversion of MO are achieved at relatively low residence times for batch experiments with comparable selectivity of epoxide [34]. To identify the optimal values of the factors influencing conversion and selectivity, DoE is used. The linear and quadratic influences of the factors on conversion and selectivity are studied and a prediction of the responses is made using FCCC/design. The values of the predicted model from Modde 10.1 are comparable to the experimental results for batch experiments.

### Table 9

| Phase ratio | $k_{\text{app}}$ in min$^{-1}$ | Average Selectivity Epoxide in % |
|-------------|--------------------------------|----------------------------------|
| 3           | 0.181                          | 26.3                             |
| 7           | 0.175                          | 33.4                             |

### Table 10

| Phase ratio | $k_{\text{app}}$ in min$^{-1}$ | Average Selectivity Epoxide in % |
|-------------|--------------------------------|----------------------------------|
| 3           | 0.174                          | 27.6                             |
| 7           | 0.179                          | 34.0                             |
With the optimal values from batch experiments as a reference, the feed for the continuous system is prepared after considering the changes involved in calculating the material quantity ratios of flow variables. Experiments are performed to identify the effect of continuous mode parameters on the conversion and selectivity of the reaction system. The effect of the phase ratio of organic to the aqueous phase, the total volumetric flow rate of the reaction system, and the differences in the slug length are studied by changing one parameter for an experiment while the other two parameters are kept constant. The maximum length of the reactor used is 15 m. A 3-way valve is placed at different lengths of the reactor, to obtain samples and to monitor the progress of the reaction. Samples are collected for analysis only after a steady state of flow is achieved. The phase ratio, total volumetric flow rate, and the pressure in the system are observed continuously. Experiments proved that each of the above-mentioned parameters influences the conversion and selectivity of the reaction system. Plots are constructed to understand the progress of the reaction along the length of the reactor. It is proven that high conversion of MO and desirable selectivity of epoxide is reached at lower residence time (10 min) in comparison to the batch experiments (3 h).

The results suggest the possibility to control conversion and selectivity of the continuous reaction employing slug length, phase ratio, and total flowrate as actuating variables. However, the effects individual slug flow parameters have on the reaction outcome are not as clear and intuitive as initially assumed. Especially the trends observed for selectivity are difficult to explain simply with changes in interfacial area and internal mixing behaviour of the slug flows, remaining rather elusive. Considering the residence time of reactants in the reactor and the resulting system inertia, predictions about the system trajectory are likely necessary to control it effectively. Thus, a model of the slug flow reactor must be constructed. While physical (e.g. CFD) models of the slug flow regime have been constructed in the past [18] and their extension to include the reaction conducted in this work appears as a possibility, models for control purposes must be executable in real-time, limiting the possible complexity. Therefore, the creation of a data-based model using machine learning algorithms appears as a promising alternative capable of predicting the outputs of a system from a multitude of possible inputs, detached from the unclear physical basis.

Appendix B – Working principle of DoE (Modde 10.1)

The DoE proceeds stepwise. At first, screening of the factors takes place followed by the optimization objective. Screening of the factors is done at first to find those factors that influence both linear and interaction models. Linear models describe the influence of a single factor on the reaction system. If the linear model shows a value in the positive region of the plot, then the increase in the factor increases the responses given to a system. An interaction model explains the strength in the relation between an independent and dependent factor, as a function of other independent factors. After the screening of factors, the optimization mode is activated. The factors are entered as inputs with upper and lower limits.

Appendix C—Comparison of the number of experiments between conventional design and FCCC design

| Number of Factors | Number of experiments for conventional design | Number of experiments for FCCC-design |
|-------------------|----------------------------------------------|-------------------------------------|
| 2                 | 9                                            | 8                                   |
| 3                 | 27                                           | 14                                  |
| 4                 | 81                                           | 24                                  |
| 5                 | 243                                          | 26                                  |
| 6                 | 729                                          | 44                                  |
| 7                 | 2187                                         | 78                                  |

Appendix A—Experimental procedure for batch mode

The procedure for the batch experiments are as follows: At first, H2O2 is added to the system. The amount of H2O2 required is calculated using the molar ratio of H2O2 to MO. Then, Aliquat ® 336 is loaded to the reaction medium followed by the addition of 1.5 g of MO. TPA is added to the system, therefore the catalytic complex synthesis is carried out in-situ. The experiments are carried out for different reaction times, stirrer speeds, and temperatures. The reaction is quenched in an ice bath after the reaction duration. Once the reaction is quenched, analysis of the aqueous and organic phases for selectivity and conversion determination is carried out with the help of Gas Chromatography.
**Appendix D – Batch DOE experiments & results**

Table 12  Results of batch experiments

| Exp. No | Temperature [°C] | PTC:C [-] | MO:C [-] | H2O2:MO [-] | Stirrer [RPM] | Time [h] | X_MO [%] | S_Epo [%] | S_Diol [%] |
|---------|------------------|-----------|----------|-------------|---------------|----------|----------|-----------|-----------|
| 1       | 50               | 6         | 50       | 1           | 100           | 1        | 42       | 35        | 16        |
| 2       | 50               | 1         | 200      | 1           | 100           | 1        | 28       | 55        | 8         |
| 3       | 50               | 6         | 50       | 4           | 100           | 1        | 38       | 34        | 17        |
| 4       | 50               | 1         | 200      | 4           | 100           | 1        | 16       | 49        | 14        |
| 5       | 50               | 1         | 50       | 1           | 600           | 1        | 8        | 23        | 21        |
| 6       | 50               | 6         | 200      | 1           | 600           | 1        | 53       | 51        | 20        |
| 7       | 50               | 1         | 50       | 4           | 600           | 1        | 35       | 48        | 16        |
| 8       | 50               | 6         | 200      | 4           | 600           | 1        | 97       | 42        | 29        |
| 9       | 80               | 1         | 50       | 1           | 100           | 1        | 19       | 51        | 23        |
| 10      | 80               | 6         | 200      | 1           | 100           | 1        | 46       | 48        | 18        |
| 11      | 80               | 1         | 50       | 4           | 100           | 1        | 34       | 64        | 24        |
| 12      | 80               | 6         | 200      | 4           | 100           | 1        | 35       | 62        | 21        |
| 13      | 80               | 6         | 50       | 1           | 600           | 1        | 50       | 31        | 18        |
| 14      | 80               | 1         | 200      | 1           | 600           | 1        | 48       | 41        | 25        |
| 15      | 80               | 6         | 50       | 4           | 600           | 1        | 89       | 36        | 26        |
| 16      | 80               | 6         | 200      | 4           | 600           | 1        | 89       | 41        | 29        |
| 17      | 50               | 1         | 50       | 1           | 100           | 5        | 37       | 15        | 16        |
| 18      | 50               | 6         | 200      | 1           | 100           | 5        | 56       | 44        | 21        |
| 19      | 50               | 1         | 50       | 4           | 100           | 5        | 60       | 16        | 6         |
| 20      | 50               | 6         | 200      | 4           | 100           | 5        | 39       | 31        | 15        |
| 21      | 80               | 6         | 50       | 1           | 100           | 5        | 49       | 27        | 14        |
| 22      | 80               | 1         | 200      | 1           | 100           | 5        | 28       | 46        | 13        |
| 23      | 80               | 6         | 50       | 4           | 100           | 5        | 76       | 33        | 18        |
| 24      | 80               | 1         | 200      | 4           | 100           | 5        | 54       | 42        | 16        |
| 25      | 65               | 1         | 125      | 2.5         | 350           | 3        | 85       | 40        | 26        |
| 26      | 65               | 6         | 125      | 2.5         | 350           | 3        | 98       | 43        | 29        |
| 27      | 65               | 3.5       | 50       | 2.5         | 350           | 3        | 92       | 43        | 27        |
| 28      | 65               | 3.5       | 200      | 2.5         | 350           | 3        | 98       | 46        | 31        |
| 29      | 65               | 3.5       | 125      | 1           | 350           | 3        | 56       | 53        | 21        |
| 30      | 65               | 3.5       | 125      | 4           | 350           | 3        | 64       | 46        | 20        |
| 31      | 65               | 3.5       | 125      | 2.5         | 350           | 1        | 57       | 50        | 22        |
| 32      | 65               | 3.5       | 125      | 2.5         | 350           | 5        | 91       | 23        | 21        |
| 33      | 65               | 3.5       | 125      | 2.5         | 350           | 3        | 94       | 34        | 23        |
| 34      | 80               | 1         | 50       | 1           | 600           | 5        | 38       | 30        | 32        |
| 35      | 50               | 6         | 50       | 1           | 600           | 5        | 61       | 40        | 20        |
| 36      | 50               | 1         | 200      | 1           | 600           | 5        | 54       | 42        | 20        |
| 37      | 80               | 6         | 200      | 1           | 600           | 5        | 53       | 58        | 23        |
| 38      | 80               | 1         | 50       | 4           | 600           | 5        | 49       | 47        | 20        |
| 39      | 50               | 6         | 50       | 4           | 600           | 5        | 99       | 16        | 21        |
| 40      | 50               | 1         | 200      | 4           | 600           | 5        | 98       | 21        | 25        |
| 41      | 80               | 6         | 200      | 4           | 600           | 5        | 98       | 31        | 25        |
| 42      | 50               | 3.5       | 125      | 2.5         | 350           | 3        | 98       | 39        | 25        |
| 43      | 80               | 3.5       | 125      | 2.5         | 350           | 3        | 95       | 34        | 21        |
| 44      | 65               | 3.5       | 125      | 2.5         | 350           | 3        | 98       | 35        | 25        |
| 45      | 65               | 3.5       | 125      | 2.5         | 350           | 3        | 90       | 39        | 24        |
| 46      | 65               | 2.5       | 100      | 3           | 600           | 3        | 91       | 42        | 22        |
| 47      | 65               | 2.5       | 600      | 3           | 600           | 3        | 98       | 39        | 24        |
Fig. 20 DoE response contour for MO conversion at constant Temperature and MO:C ratio

Fig. 21 DoE response contour for selectivity toward epoxide at constant PTC:C and H2O2:MO ratios
Table 13  DoE model parameters for conversion

| Conversion | Coeff. SC | Std. Err | P       | Conf. int(±) |
|------------|-----------|----------|---------|--------------|
| Constant   | 92,732    | 369,441  | 4.95E-11| 773,258      |
| Temperature| 0,489,048 | 182,681  | 0,791,809| 38,236       |
| PTC:C      | 792,215   | 182,681  | 0,000,355,472| 38,236      |
| MO:C       | 31,982    | 182,681  | 0,961,268| 38,236       |
| H2O2:MO    | 910,941   | 182,681  | 8,19E-01 | 38,236       |
| Stirrer speed | 931,581   | 182,681  | 6,37E+00 | 38,236       |
| Time       | 632,379   | 182,681  | 0,002,61,295| 38,236      |
| Temp*Temp  | -315,342  | 593,677  | 0,601,458| 12,426       |
| PTC:C*PTC:C| -390,997  | 593,677  | 0,518,053| 124,259      |
| MO:C*MO:C  | -321,256  | 593,677  | 0,594,707| 124,259      |
| H:MO*H:MO  | -919,171  | 593,677  | 0,138,053| 124,259      |
| StiSp*StiSp| -340,554  | 593,677  | 0,572,943| 124,259      |
| Time*Time  | -707,038  | 593,677  | 0,248,341| 12,426       |
| Temp*PTC:C | 0,00,040,674| 161,889  | 0,954,438| 38,236       |
| Temp*MO:C  | -0,937,288| 161,889  | 0,363,314| 38,236       |
| Temp*H:MO  | 150,789   | 161,889  | 0,688,341| 38,236       |
| Temp*StiSp | -659,374  | 161,889  | 0,291,867| 38,236       |
| Temp*Time  | -381,889  | 161,889  | 0,215,214| 38,236       |
| PTC:C*MO:C | -4,055    | 161,889  | 0,730,945| 38,236       |
| PTC:C*H:MO | -0,564,956| 161,889  | 0,258,603| 38,236       |
| PTC:C*StiSp| 188,533   | 161,889  | 0,510,857| 38,236       |
| PTC:C*Time | -108,482  | 161,889  | 0,730,968| 38,236       |
| MO:C*StiSp | -528,041  | 161,889  | 0,410,394| 38,236       |
| MO:C*Time  | -174,437  | 161,889  | 0,294,744| 38,236       |
| H:MO*StiSp | 584,592   | 161,889  | 0,001,861| 38,236       |
| H:MO*Time  | 155,648   | 161,889  | 0,348,405| 38,236       |
| StiSp*Time | -174,513  | 161,889  | 0,294,539| 38,236       |
| N = 47     | Q2 = 0,720| Cond. no. = 10,35 |
| DF = 19    | R2 = 0,917| RSD = 12,39 |
| Comp. = 3  | R2 adj. = 0,799| Conf. lev. = 0,95 |
| Table 14 DoE model parameters for selectivity |
| Selectivity | Coeff. SC | Std. Err | P | Conf. int(±) |
| Epoxide | | | | |
| Constant | 409,174 | 241,487 | 6.34E-08 | 505,443 |
| Temperature | 346,038 | 11,941 | 0,00,922,114 | 249,931 |
| PTC:C | -0,55078 | 11,941 | 0,649,854 | 249,931 |
| MO:C | 432,015 | 11,941 | 0,0,018,322 | 249,931 |
| H2O2:MO | -126,586 | 11,941 | 0,30,239 | 249,931 |
| Stirrer speed | -116,448 | 11,941 | 0,341,716 | 249,931 |
| Time | -479,787 | 11,941 | 0,00,735,357 | 249,931 |
| Temp*Temp | -100,679 | 11,941 | 0,798,084 | 812,226 |
| PTC:C*PTC:C | -0,251,094 | 11,941 | 0,949,086 | 249,931 |
| MO:C*MO:C | 0,159,932 | 11,941 | 0,967,086 | 812,226 |
| StiSp*StiSp | -0,421,675 | 11,941 | 0,775,345 | 812,226 |
| Time*Time | -0,975,931 | 11,941 | 0,804,135 | 812,226 |
| MO:C | 432,015 | 11,941 | 0,0,018,322 | 249,931 |
| MO:MO | -126,586 | 11,941 | 0,30,239 | 249,931 |
| MO:C | 432,015 | 11,941 | 0,0,018,322 | 249,931 |
| MO:C | 432,015 | 11,941 | 0,0,018,322 | 249,931 |
| MO:C | 432,015 | 11,941 | 0,0,018,322 | 249,931 |
| MO:C | 432,015 | 11,941 | 0,0,018,322 | 249,931 |
| MO:C | 432,015 | 11,941 | 0,0,018,322 | 249,931 |
| MO:C | 432,015 | 11,941 | 0,0,018,322 | 249,931 |

Besides, the volume flow of components must be included in the calculation of material quantity ratios in the reactor. A change in the ratio of the volume flow of feed affects the mass flow of the system. 200 g of 70% MO is taken as the basis for continuous experiments. Therefore, the volume of the feed system is calculated as a function of the density of the individual component (ρ).

Where m is the mass of the component under consideration. Based on the above equation, the volume of MO considered for continuous experiments is found to be ~229 ml (0,47 mol). ~1 molar equivalent of H2O2 is sufficient for epoxidation of MO through batch experiments, according to Table 2. The corresponding volume of H2O2 required for epoxidation of MO is determined using Eq. 10. A phase ratio of 5 between the organic and aqueous phases, is required for the epoxidation of MO based on volume flow.

Due to the higher solubility levels of TPA in water [35], it is mixed with 35% H2O2 as an aqueous system. Aliquat® 336, an organic compound, is soluble in systems containing a higher number of carbon atoms. Therefore, it is mixed with MO as the organic feed system. The amount of TPA and Aliquat® 336 required to complete the feed system is calculated with the help of molar ratios of PTC/C and MO/C from Table 2. The feed systems are continuously stirred to ensure proper mixing of the chemicals.

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