Sensitivity of nonlinear photoionization to resonance substructure in collective excitation

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Collective behaviour is a characteristic feature in many-body systems, important for developments in fields such as magnetism, superconductivity, photonics and electronics. Recently, there has been increasing interest in the optically nonlinear response of collective excitations. Here we demonstrate how the nonlinear interaction of a many-body system with intense XUV radiation can be used as an effective probe for characterizing otherwise unresolved features of its collective response. Resonant photoionization of atomic xenon was chosen as a case study. The excellent agreement between experiment and theory strongly supports the prediction that two distinct poles underlie the giant dipole resonance. Our results pave the way towards a deeper understanding of collective behaviour in atoms, molecules and solid-state systems using nonlinear spectroscopic techniques enabled by modern short-wavelength light sources.

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Significant advancements in photonics, especially in electric field enhancement and harmonic generation, have been mostly triggered by the recent development in tailoring materials on the nanometre scale exploiting their resonant collective response to radiation. To optimize the coupling between the nanostructure and the electromagnetic field, a detailed understanding of the underlying resonant response is essential. To this end, atomic samples provide a valuable benchmark for understanding more complex systems, easing meaningful systematic investigations.

An illustrative example of a many-body system showing collective electronic behaviour is atomic xenon, its resonant character under extreme ultraviolet (XUV) radiation, known as the 4d giant dipole resonance, is interpreted as the collective response of many electrons to an external weak-field perturbation. The recent advent of high-brilliance light sources such as XUV and X-ray free-electron lasers (FELs) has opened a door to XUV and X-ray studies beyond the linear regime. Exploiting this new high-intensity technology renders it possible to investigate the collective response mechanisms of many-body systems through their nonlinear interaction with short-wavelength radiation. As shown here, this provides the possibility of unveiling substructures in the spectrum of collective excitations that cannot be resolved with linear spectroscopy.

The case of xenon ionization under the unprecedented conditions at FELs has been the subject of several investigations, which have stimulated speculations about the influence of collective effects on the process of multiple excitations. Many-body systems through their nonlinear interaction with the ionization of xenon, opened a door to XUV and X-ray studies beyond the linear regime. An illustrative example of a many-body system showing collective behaviour is atomic xenon, its resonant character under extreme ultraviolet (XUV) radiation, known as the 4d giant dipole resonance, is interpreted as the collective response of many electrons to an external weak-field perturbation. The recent advent of high-brilliance light sources such as XUV and X-ray free-electron lasers (FELs) has opened a door to XUV and X-ray studies beyond the linear regime. Exploiting this new high-intensity technology renders it possible to investigate the collective response mechanisms of many-body systems through their nonlinear interaction with short-wavelength radiation. As shown here, this provides the possibility of unveiling substructures in the spectrum of collective excitations that cannot be resolved with linear spectroscopy.

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Results

Experiment and theory approach to nonlinear photoionization. Our findings are made possible by the combination of electron spectroscopy, which allows the disentanglement of photoemission processes from different orders of interaction, with first-principles calculations. We measured the relative yields of 1-photon and 2-photon ionization of the 4d shell of xenon (Fig. 1a,b) by electron spectroscopy and compare them with numerical solutions of the many-electron Schrödinger equation for atomic xenon in the presence of an external XUV laser field. Our theoretical model captures many-body processes beyond linear response theory, allowing the selective inclusion of those electronic correlation effects that are responsible for collectiveness. For a system characterized by collective behaviour, the wavefunction is given by a coherent superposition of particle-hole states, due to the strong particle-hole interaction. We compare the experimental results with the full model, which describes the collective response of the system by accounting for the electron–hole interaction in all channels open to ionization (Fig. 1d), and a reduced model, which confines this interaction to the hole from which the electron was excited (Fig. 1c).

Electron spectroscopy of 1- and 2-photon ionization. Our experiments were performed at the BL2 beamline of FLASH, the Free-electron LASer in Hamburg, Germany. FEL pulses at photon energies of 105 and 140 eV were focused down to a few microns in front of the aperture of a magnetic bottle electron spectrometer. The spectrometer was used to measure the kinetic energy (KE) of the electrons produced by 1-photon and 2-photon absorption processes in an effusive jet of xenon atoms (see Methods).

Electron spectra (Fig. 2) were collected under different intensity conditions. The spectra include features caused by 1-photon direct emission from the 5p, 5s and 4d shells as well as from NOO Auger decay. At higher kinetic energies, the 2-photon ionization from the 4d shell is observed in a spectral feature that resembles in shape the 4d (1-photon) emission lines and is separated from them by exactly the energy of one photon.

The relative yields from the 4d 1- and 2-photon ionization processes are obtained by integrating the spectra over the corresponding kinetic energy regions (105 eV, 1-photon: 140 eV, 2-photon).
Comparison between experimental and theoretical results. The experimental yields are compared with the results of calculations performed for the full and the reduced models, respectively. This comparison clearly shows that the full model reproduces the intensity dependence of the experimental yields, whereas the reduced model fails to do so. This means that the inclusion of Coulomb coupling between all possible electron–hole states, which is responsible for the collective electronic response of the system, is an essential ingredient for the correct description of the 2-photon ionization process. The very good agreement is evident in the ratio between the 1-photon and 2-photon ionization yields at both photon energies over the whole intensity range as well as in the onset of the saturation due to neutral target depletion.

Discussion

Having validated our full model by the comparison with experimental yields at two photon energies, we investigate the influence of collective effects on the 1- and 2-photon ionization cross-section over a wide photon energy range (Fig. 4). For the 1-photon cross-section, the broadening is due to the well-known broadening and blue shift of the giant resonance caused by the
while at 105 eV it is larger by a factor of 2.2. Further analysis simultaneously at 105 and 140 eV, by the two-step picture with underlying the giant resonance 22. These states give rise to this substructure, which emerges in the nonlinear process, into the continuum decreases monotonically with increasing energy. This model captures qualitatively the behaviour of the cross-section for exciting an electron from the intermediate state, one expects a narrower 2-photon peak that is shifted to lower energy (dash–dotted blue curve), since the 1-photon cross-section curve produced by the reduced model can be qualitatively understood (Fig. 4a) in terms of a sequential process involving a single intermediate state, where the 2-photon cross-section (red-dotted curve) factorizes into two 1-photon cross-sections (one photon for exciting the giant resonance from the ground state (solid black curve), and the other photon for the transition from the resonance to the final state, which is modelled by a $E^{-13/2}$ energy dependence (see Supplementary Discussion)). According to this two-step picture with a single intermediate state, one expects a narrower 2-photon peak that is shifted to lower energy (dash–dotted blue curve), since the 1-photon cross-section for exciting an electron from the intermediate state into the continuum decreases monotonically with increasing energy. This model captures qualitatively the behaviour of the 2-photon cross-section in the reduced model case. In contrast, for the full model (Fig. 4b), the picture of a sequential process involving a single intermediate state does not hold: surprisingly, the 2-photon cross-section curve is much broader than the 1-photon cross-section curve and exhibits a knee-type structure. This substructure, which emerges in the nonlinear process, manifests the existence of more than one resonance state underlying the giant resonance22. These states give rise to interference terms resulting in a broadening of the 2-photon absorption cross-section curve (see Supplementary Discussion). Indeed, the experimental results cannot be explained, simultaneously at 105 and 140 eV, by the two-step picture with a single intermediate state (dash–dotted blue curve). In particular, at 140 eV the cross-section measured experimentally is ~12 times larger than predicted by the single intermediate state model, while at 105 eV it is larger by a factor of 2.2. Further analysis within the time-dependent configuration interaction singles scheme (TDCIS) reveals two underlying resonance states26, which are indicated by arrows in the inset of Fig. 4b. The resonance positions are consistent with the substructure visible in the 2-photon cross-section. Here for the first time, the agreement of a theoretical model with experimental results beyond the linear regime legitimates the prediction of two resonances underlying the giant resonance22.

Summarizing, we have shown that the nonlinear response of an electronic system to intense XUV radiation can be used to unveil information about the collective behaviour in many-body systems. The theoretical xenon 2-photon cross-section exhibits a knee-type structure that is not visible in the 1-photon cross-section. The present study demonstrates, employing xenon as a model system, how the nonlinear interaction regime can be utilized to investigate collective electronic behaviour. This stands only at the beginning of the way towards a deeper understanding of the collective response of many-body systems.

**Methods**

**FEL beam transport and characteristics.** The self-amplified spontaneous emission FEL pulses had a duration of about 80 ± 20 fs and up to 40 µJ (at 105 eV) and 15 µJ (at 140 eV) energy per pulse. The bandwidth was about 1% at both photon energies. The FEL pulses were focused onto the sample by means of MoB,C multilayer mirrors in a back-reflecting geometry to produce a tight focusing of about 5 ± 1 µm full width at half maximum. The mirrors have a reflection bandwidth of ~1 eV with peak reflectivity of ~40% (at 105 eV) and ~20% (at 140 eV) centred at the respective photon energy, thus enabling in addition a very effective filtering (>4 orders of magnitude) of any possible higher harmonic contamination (estimated < 0.3%) FEL irradiance press tuned using a gas attenuator system and moving the focusing mirror along the beam direction in order to vary the beam cross-section within the interaction zone. The attenuator was used to control the energy per pulse delivered into the interaction region thereby providing a fine tuning of the intensity over a restricted range (~1 order of magnitude). In addition, by varying the beam cross-section from the minimum value of 5 µm up to ~190 µm, the intensity was altered over more than 4 orders of magnitude. The photon beam parameters were monitored online during the experiments. A calibrated gas monitor detector provided the energy of the FEL pulses on a single-shot basis24. A charge-coupled device camera was used to record the single-shot FEL spectra from a variable line spacing grating spectrometer installed along the beam transport. The spectral information was used to normalize the beam intensity to the multilayer mirror reflection curve.

**Electron spectroscopy for determining experimental yields.** Electron spectra of 1-photon and 2-photon ionization of xenon were measured by means of a magnetic bottle electron spectrometer (MBES)27. Technically, since the photon energies exceed the binding energy of the orbital under consideration, the observed 2-photon process is above-threshold ionization. The acceptance volume of the MBES, limited by the magnetic field lines of the system, had a size of ~0.5 mm in the plane perpendicular to the spectrometer axis. The MBES enables 4π acceptance of the solid angle with an energy resolution for the detected electrons of 2%. By means of a retardation stage, it was possible to increase the resolution of the spectral features down to the FEL bandwidth limit. The 1-photon and 2-photon signals were collected for different FEL intensities under different MBES settings as well as different conditions for the sample density. 2-Photon electrons were collected under higher sample density conditions and applying a retarding field at the entrance of the MBES rejecting slow electrons, to avoid detector saturation induced by the 1-photon signal. The intensity-independent normalization factors defining the relative yields (sample density, transmission of the analyser and detector gain) are calibrated by comparing the experimental and theoretical results obtained for the 1-photon and 2-photon ionization from the 3p orbital of argon, which is a much less complex system exhibiting negligible correlation effects, thereby providing a robust calibration reference.

The experimental intensity domains are not identical for the the 1-photon and the 2-photon yields, collected in subsequent measurements, because of the consistent varying of the self-amplified spontaneous emission FEL intensity during the shifts. For the 105 eV case, where electron yields are more severely affected by saturation effects at high intensities, the experiment was performed under different focusing conditions to allow the investigation over a broader intensity range. The experimental yields are extracted by integrating the FEL intensity-resolved electron spectra in the KE regions mentioned in the Results section, corresponding to the binding energy ranges from 66 to 72 eV and from 64 to 74 eV for the 1-photon and the 2-photon signals, respectively.
Data acquisition. Electron energy spectra were acquired by feeding the signal from the detector collection anode into a Leccoy WavePro 7253iA digital oscilloscope (8 bit, 10 GSPS, 2.5 GHz bandwidth) triggered by a transmitter–transistor logic signal synchronized with the FEL pulse. The DAQ server was controlled by a Labview-based data acquisition (DAQ) client enabling the collection of single-shot spectra and their sorting according to the intensity and the spectral distribution of the FEL. Intensity-resolved electron energy spectra can be extracted in two different ways depending on the energy threshold chosen. Low-KE spectra, produced by single-photon processes, result from the analogue current signal collected by the detector anode. The 2-photon direct ionization features, with yields that are some orders of magnitude lower than the 1-photon features, result from the collection of only a few electrons per FEL shot by the detector. Their signal is time discriminated by software, and the histogram of their arrival time is taken in counting mode and suitably normalized, resulting in a virtually background-free electron spectrum. This approach enables the extension of the dynamic range well beyond the limitation given by the digitizer.

First-principles calculation of cross-sections. Our model is based on the TDCCIS\(^5\). In this nonperturbative approach the full N-electron Schrödinger equation is solved numerically:

\[
\frac{\partial}{\partial t} |\Psi(t)\rangle = H(t) |\Psi(t)\rangle. \tag{1}
\]

The wavefunction is expanded in the one-particle–one-hole basis:

\[
|\Psi(t)\rangle = x_0(\tau)|\Phi(0)\rangle + \sum_i x_i(\tau)|\Phi_i(\tau)\rangle, \tag{2}
\]

where the index \(i\) denotes an initially occupied orbital, \(\alpha\) stands for an unoccupied orbital and \(|\Phi(0)\rangle\) symbolizes the Hartree–Fock ground state. The cross-sections for 1- and 2-photon absorption are calculated via the population in the corresponding hole channels, which are distinguishable due to the different angular momenta of the ejected electron. The level of our calculations does not include any ground-state correlations. Within TDCCIS it is possible to include and distinguish certain electronic correlation effects that are mediated by Coulomb interaction. In particular, for the description of a collective response, the system cannot be described by a single particle–hole state, but rather a superposition of particle–hole states is needed. The full model includes the coupling among the holes in the 4d, 5s and 5p orbitals and the electron. The corresponding Coulomb matrix elements \(\langle \Phi_i|\hat{H}_{\text{Coulomb}}|\Phi_0\rangle\) are included for all different index pairs within the space of active orbitals. In this way, superpositions of particle–hole states, that is, collective states, may be described. In contrast, in the case of the reduced model the elements with \(i \neq j\) are set to zero, which results in the description of coupling only with the very 4d orbital from which the electron was ionized.

Rate equations for theoretical yield calculation. The theoretical yields are obtained from the numerical solution of equations (3–7) valid for the electron yield from the neutral target (population \(N_0\)).

\[
\frac{dN(t)}{dt} = -y_{1ph}(t) - y_{2ph}(t) \tag{3}
\]

\[
y_{1ph}(t) = \sigma^{(1)} \cdot j(t) \cdot N_0(t) \tag{4}
\]

\[
y_{2ph}(t) = \sigma^{(2)} \cdot j(t) \cdot N_0(t) \tag{5}
\]

\[
Y_{1ph} \equiv \int dt \, y_{1ph}(t) \tag{6}
\]

\[
Y_{2ph} \equiv \int dt \, y_{2ph}(t) \tag{7}
\]

Rate equations are solved assuming a Gaussian pulse with 80 fs (full width at half maximum) duration. \(\sigma^{(1)} (1\text{-photon})\) and \(\sigma^{(2)} (2\text{-photon})\) ionization cross-sections entering equations (4) and (5) are obtained for the full and the reduced model as described above. The rate equation solutions \(Y_{1ph}\) and \(Y_{2ph}\) are calculated over a very broad range (9 orders of magnitude) of laser intensities and the results are numerically integrated over the volume of acceptance of the electron analyser in order to account for the spatial distribution of the FEL fluence.

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