Genome analysis

**Dot2dot: accurate whole-genome tandem repeats discovery**

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Associate Editor: John Hancock

Received on March 30, 2018; revised on August 3, 2018; editorial decision on August 23, 2018; accepted on August 24, 2018

Abstract

**Motivation:** Large-scale sequencing projects have confirmed the hypothesis that eukaryotic DNA is rich in repetitions whose functional role needs to be elucidated. In particular, tandem repeats (TRs) (i.e. short, almost identical sequences that lie adjacent to each other) have been associated to many cellular processes and, indeed, are also involved in several genetic disorders. The need of comprehensive lists of TRs for association studies and the absence of a computational model able to capture their variability have revived research on discovery algorithms.

**Results:** Building upon the idea that sequence similarities can be easily displayed using graphical methods, we formalized the structure that TRs induce in dot-plot matrices where a sequence is compared with itself. Leveraging on the observation that a compact representation of these matrices can be built and searched in linear time, we developed **Dot2dot:** an accurate algorithm fast enough to be suitable for whole-genome discovery of TRs. Experiments on five manually curated collections of TRs have shown that **Dot2dot** is more accurate than other established methods, and completes the analysis of the biggest known reference genome in about one day on a standard PC.

**Availability and implementation:** Source code and datasets are freely available upon paper acceptance at the URL: https://github.com/Gege7177/Dot2dot.

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**Supplementary information:** Supplementary data are available at [Bioinformatics](/)]

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1 Introduction

A tandem repeat (TR) consists in a certain number of copies of a (typically small) motif sequence that occur adjacent to each other. More realistic definitions admit a certain degree of heterogeneity among copies of the motif sequence as well as tiny insertions or deletions. The abundance of these structures in eukaryotic DNAs has been observed since the first sequencing data became available in the early 90s (Bacolla et al., 2008). Although TRs functional role is not completely understood yet, their distribution in eukaryotic genomes suggests involvement in several cellular processes including gene expression (Tóth et al., 2000). Besides confirming this thesis, the steady growth of the number of genetic disorders related to the expansion of TRs has kindled the hope of associating TRs polymorphism with the etiology of those genetic diseases that are still unexplained. This trend led the bioinformatics community to focus on research projects aimed at a large-scale analysis of repetitions. Unfortunately, validating a new relevant TR can be as difficult as finding a needle in the haystack and the success of these projects heavily depends on the sensitivity of the searching algorithms. The difficulty of capturing the variability of satellites and microsatellites into a single comprehensive computational model has encouraged researchers to design new methods for large-scale TR discovery.
Nevertheless, an agreed computational model for non-naive biologically relevant TRs is still far away.

According to different searching strategies and definitions of TRs, several algorithm families have been proposed. Dictionary-based methods (Castelo et al., 2002; Delgrange and Rivals, 2004; Karaca et al., 2005; Parisi et al., 2003; Pokrzywa and Polanski, 2010) leverage on a pre-determined set of seeds that is searched along the input sequence and subsequently expanded. This class of algorithms is particularly efficient in those situations where the user is interested in a relatively small class of repeats. Exhaustive search of TRs, instead, is unaffordable because of the exponential growth of the dictionary size as a function of the allowed motif length. The dual approach is that of ab-initio methods (Benson, 1999; Boeva et al., 2006; Girgis and Sheetlin, 2013; Koller et al., 2007; Kolpakov et al., 2003; Krishnan and Tang, 2004; Kurtz et al., 2001; Pellegrini et al., 2010; Sokol et al., 2007; Wexler et al., 2005; Wirawan et al., 2010; Zhou et al., 2009) that do not require any pre-existing knowledge about the input sequence. Although more complex, this class of algorithms is the most studied and used in practice.

The presence of variations (single nucleotide polymorphisms, insertions and deletions) in the genomes has directed many researchers to develop algorithms in which the distance between units of a motif is based on the Needleman–Wunsch sequence alignment algorithm described in Needleman and Wunsch (1970). The high quadratic cost of this procedure, however, has convinced researchers to shift to algorithms that work in Hamming distance. Hybrid approaches use Hamming distance instead of sequence alignment but allow insertions between consecutive copies of the motif.

Output filtering is a desirable but not mandatory feature of TR searching methods. Its main advantage is the elimination/reduction of redundancy often caused by software artifacts. Aggressive filtering, however, can cause the removal of relevant results and, as a consequence, the reduction of the algorithm accuracy.

Two distinguishing features have recently gained importance: the ability of managing multi-sequence files coming from NGS sequencing and the possibility of scanning entire assembled genomes. Both these features can involve a potentially huge amount of data and thus require fast algorithms that avoid computationally expensive operations without sacrificing output quality.

In this paper, we present Dot2dot, a novel algorithm for TR discovery. Our method borrows some ideas from a widely used tool to visually display local alignments between pairs of sequences, namely dot-plots. In particular, we observed that aligning a sequence with itself, TRs form a regular pattern. Our algorithm mimics such visual search for these patterns to accomplish TR discovery. One of the main novelties of our approach is a compact representation of the dot-plot matrices that: (i) allows us to scale at genome-wide analysis, and (ii) can find application to other problems where dot-plots are used. Our algorithm belongs to the class of ab-initio methods, it allows both a tunable degree of divergence from the consensus sequence and a small insertion between two consecutive motifs. Both fasta and fastq are accepted as input allowing the analysis of NGS sequences. Dot2dot implements an optional customizable filter able to: remove biologically irrelevant results, and control the degree of overlap among TRs in the output list. Under the sensible assumption that the longest TR in the input sequence is much shorter (by orders of magnitude) than the entire sequence, our algorithm runs in linear time, thus enabling the analysis at whole-genome scale. Besides designing a new searching algorithm, we built five testing datasets covering diverse applicative areas. In particular: we collected from several public sources a set of 45 validated pathology-linked TRs; we compiled the list of coordinates of the CODIS loci including the seven loci that have been added since January 2017; we mapped on the hg38 reference genome a set of 620 manually annotated TRs reported in the Marshfield panel of variable loci; and we computed a catalog of 15 326 TRs located in upstream regulatory regions.

2 Materials and methods

Our algorithm leverages on a data structure at the base of dot-plots. Dot-plots are used to gain a visual insight of local alignments between two different sequences or even a sequence against itself. Matches between two elements are represented as (typically black) spots. A natural extension of this visual representation of alignments allows the use of color graduation to represent degree of similarity between pairs of elements (Somhammer and Durbin, 1995). The underlying data structure (called dot matrix) is a matrix where the element M[i, j] stores the degree of similarity between the character in position i of the first sequence and the element in position j of the other string. When a sequence s is aligned with itself, M[i, i] stores the degree of similarity between the element in position i and that in position j of s.

We observed that TRs form a distinctive pattern on self-sequence alignment dot-plots and, in turn, this pattern reflects on the underlying dot matrix. Consider e.g. a pure TR, since each instance of the motif perfectly aligns with the first instance, it will form a diagonal on the dot-plot. All these diagonals will lie stacked over the main diagonal. Counting the number of stacked diagonals we compute the number of copies of the consensus sequence, while from the length of the diagonals we derive the motif length. Fuzziness of TRs can easily be captured within this model. In fact, mismatches correspond to gaps in the diagonals, deletions cause interrupted diagonals and insertions cause the shift of the remaining part of the TR (see examples in the Supplementary Material). We noticed that the presence in the dot matrix of the above described pattern is a necessary and sufficient condition for the existence of a tandemly repeated sequence in the input, thus an algorithm that locates all and only these patterns ensures a computationally correct and complete tool for TRs discovery.

The naive quadratic cost of building, storing and searching the dot matrix is inadequate for whole-genome analysis. In order to lower the memory consumption and speed up the computation we propose an alternative representation of this data structure that can be built and stored in linear time/space. We also propose a fast searching heuristic algorithm to enumerate all the instances of the TR pattern in the dot matrix.

2.1 Data structure

In this section we provide details on how to infer the dot matrix M without explicitly building it. Let \( S = s_1 s_2 \ldots s_n \) be a sequence of length \( n \) over a finite alphabet \( \Sigma \) (where \( \Sigma = \{A, C, G, T\} \) in our case). Given a character \( x \in \Sigma \) we define \( P(x) \) as the set of positions of \( S \) where \( s_i = x \). The comparison of the character \( x \) and the sequence \( S \) induces a row \( M[x] \) of \( M \) whose content does not depend on the position of \( x \) in the sequence but only on the content of \( S \). As a consequence, comparing the sequence \( S \) with itself, the resulting matrix \( M \) has \( |P(x)| \) rows identical to \( M[x] \).

Following the above observation, building the whole \( M \) it suffices to compute only the vector \( M[x] \) for each \( x \in \Sigma \). In order to obtain a direct positional access to the induced dot matrix we build an auxiliary vector \( V \) of length \( n \) where in position \( i \) we store a reference to \( M[s_i] \). Figure 1 shows an example data structure.

Since \( |\Sigma| \) is a constant much smaller than \( n \), building the data structure inducing \( M \) has time/space cost linearly proportional to \( n \). In fact, both \( V \) and the \( M[x] \) are vectors of size \( n \) that can be filled with a single scan of the sequence \( S \).
2.2 TR searching procedure

Searching is a relatively simple procedure that scrolls a window of fixed length along the sequence and, for each position, checks for a stacked diagonal in the matrix $M$.

Let $D_M(i, j) = \{ V[i][j], V[i+1][j+1], \ldots, V[i+l-1][j+l-1] \}$ be a $l$-long sequence of adjacent cells along $M$ starting from position $(i,j)$ such that two consecutive elements have coordinates that differ by 1 in terms of both rows and columns and let $W_M(i, j, l) = \sum_{k=0}^{l-1} V[i+k][j+k]$ be the summation of the scores of $M$ over the positions $D_M(i, j, l)$. If $W_M(i, j, l)$ is a diagonal if and only if $W_M(i, j, l) > l - \delta$ where $\delta \in [0, l]$ is a user-defined threshold. Given a certain position $i$ on the sequence $S$, the event $W_M(i, i + l, l) = l$ corresponds to a pure TR of motif length $l$ and copy number at least 2 starting from position $i$. Again $W_M(i, i + l, l) = W_M(i, i + 2l, 2l) = l$ corresponds to a pure TR with copy number at least $3$ and so on.

The parameter $\delta$ is used to control the degree of fuzziness of TRs. In fact, the event $W_M(i, i + l, l) = l - \delta$ means that the second copy of the repeat contains $\delta$ mismatches. In its simplest form, the core of our searching procedure (described in Algorithm 1) scans the sequence $S$ (see line 1) and checks for different values of $l$ (see line 2) if the event $W_M(i, i + l, l) \geq l - \delta$ is verified. When this happens, the algorithm iteratively attempts to locate further diagonals in positions $i + 2l, i + 3l$ and so on (see lines 7–10). The procedure stops when an integer $c$ such that $W_M(i, i + cl, l) < l - \delta$ is found. The sequence $S[i, i + cl]$ is reported as a TR with motif length $l$ and copy number $c$.

We further refined our procedure to deal with insertions and deletions. We restrict to the most significant class of these variants. In particular, insertions can occur only between two copies of the motif sequence and their length is limited to be lower than the motif length $l$ (see line 12). In addition, the length of insertions is fixed within the same TR. This means that, if a TR contains two or more insertions, they must have the same length to be correctly detected. Deletions are modeled as the insertion of a spurious sequence between two copies of the motif string. Although this model can appear limited, it has practical advantages and it is consistent with the replication slippage process described in Viguera et al. (2001). In fact, without a limit on the length of an insertion nearly every genomic sequence can be confused with a TR. The constraint on the equality of the insertion lengths within the same TR helps to predict the correct motif length and copy number when dealing with impure TRs. From the biological point of view, according to the model described in Viguera et al. (2001), the polymerase is arrested after replicating a unit of the repeat. Then, the realignment between the new strand and the template causes the insertion/deletion to happen between two copies of the TR motif sequence. In presence of an insertion between two copies of the consensus motif the condition $W_M(i, i + cl, l) > l - \delta$ becomes false for a certain $c$. In this case (see lines 12–16), we seek for a gap checking for a possible diagonal in at most the next $l - 1$ positions (i.e., $i + cl + 1, i + cl + 2$, etc.). In case of success we take note of the gap and its length and continue the standard searching procedure checking the next diagonal at distance $l$.

When the condition on $W()$ becomes false again we do not test all the possible sizes of the gap but only the previously annotated length.

In order to enable Dot2dot to identify the longest possible TR, the searching procedure still has to check whether the sequence immediately downstream a TR is a prefix of the consensus sequence, even though it does not satisfy the condition $W_M(i) < l - \delta$. In this case, however, we seek only for perfect matching so as not to reduce TR’s purity. We perform this test iteratively verifying (see lines 22–25) that the $i$-th character in the downstream sequence matches the $i$-th character of the motif (i.e. the first instance of the TR). If a suitable prefix is found, it is included in the output TR.

In terms of asymptotic analysis, the overall computational cost of Dot2dot is proportional to the number of times the condition $W() > l - \delta$ is tested. A single computation of $W()$ takes $O(l)$ time since it costs $l$ accesses to the matrix $M$. Given a certain position $p \in [1, |S| - 2l]$ of $S$, there are two cases: either there exists in $S$ a TR with $k_p$ copies starting in position $p$ or not. In the first case $W()$ is computed $k_p + l$ times while in the latter case $W()$ is computed only once. In general, however, $l$ is constant, but $k_p$ cannot be bounded and, thus, it can hold $k = \max_{p \in [1, |S| - 2l]}(k_p) = |S|/l$ in the worst case.

Algorithm 1 Tandem repeat searching procedure

| Require: sequence $S$, dot matrix $M$, parameter $\delta$ |
| Ensure: list $R$ of tandem repeats |
| 1: for all $i \in [1, |S|]$ do |
| 2: for all $l \in \text{range_of_motif_lengths}$ do |
| 3: $cn \leftarrow 1$; |
| 4: $gap_{offset} \leftarrow gap \leftarrow 0$; |
| 5: repeat |
| 6: $can_{extend} \leftarrow false$; |
| 7: while $W_M(i; i + gap_{offset} + (cn + l); l) < \delta - l$ do |
| 8: $cn \leftarrow cn + 1$; |
| 9: $can_{extend} \leftarrow true$; |
| 10: end while |
| 11: if $gap = 0$ then try to guess gap length |
| 12: for $k = 1$; $gap == 0$ and $k < |S|$; $k = k + 1$ do |
| 13: if $W_M(i; i + gap_{offset} + k + (cn + l); l) < \delta - l$ then |
| 14: $gap \leftarrow k$; |
| 15: end if |
| 16: end for |
| 17: end if |
| 18: $gap_{offset} \leftarrow gap_{offset} + gap$; |
| 19: until $can_{extend}$ is true; |
| 20: if $cn \geq 2$ then Found a valid TR |
| 21: $gap_{offset} \leftarrow gap_{offset} - gap$; |
| 22: last \leftarrow 0$; |
| 23: while $\text{last} < l$ and $S[i + \text{last}] = S[i + gap_{offset} + (cn + l) + \text{last}]$ do |
| 24: $\text{last} \leftarrow last + 1$; |
| 25: end while |
| 26: $R$.append $(S[i, i + gap_{offset} + (cn + l) + \text{last}], copy_{number} = cn, \text{motif}_{length} = l)$; |
| 27: end if |
| 28: end for |
| 29: end for |
case. Moreover, a similar condition can hold for every position \( p \). As a result, the overall running time of the searching procedure would be \( |S|/k = O(|S|/k) = O(|S|^2) \) in the worst case.

In terms of average-case analysis, we have to estimate the value \( \bar{k} \leq k \) that balances the high cost paid every time a new TR is found and the low cost paid otherwise. Dealing with real genomic sequences we observed that the probability for a given position to be the starting point of a TR is fairly low. Moreover, the longest TR is order of magnitude shorter than the input sequence. These assumptions would lead to an expected linear running time of our algorithm. To confirm our hypotheses we estimated the value of \( \bar{k} \) over the entire hg38 reference genome. According to our experiments we measured \( \bar{k} = 300 \) and \( \ell k = 2495 \). Moreover, the probability of a random position \( p \) to be the starting coordinate of a TR =0.0051. Consequently, the expected value of \( \bar{k} \) is 1.53.

2.3 Filtering

Exhaustive approaches to TR discovery suffer from the fact that many reported results may be artifacts rather than proper TRs. For example, finding a TR of copy number \( c \), this class of algorithms returns also all the sub-instances of copy number \( c-1, c-2, \) etc. Since this behavior has also a strongly negative impact on running time, it would be better avoiding computing these artifacts instead of filtering them a posteriori. In order to solve this problem, we maintain a bit vector to mask those positions that will certainly produce such an undesired result. Once our searching procedure identifies a new TR, it sets the bit corresponding to the first position of each copy of the motif sequence. Marked positions are ignored during the subsequent searching. We notice that this filter applies not only to pure TRs, but its benefits extend partially to fuzzy TRs. Suppose e.g. that we want to find TRs within the toy sequence \( ACG ACG ACG ACG ACG AGT AGT \) and let suppose \( \delta = 1 \). In this case, Dot2dot would return the TR \( ACG AGG ACG ACG AGC \) which is not pure because of the substitution C/G in the second copy of the motif. However, our filtering would avoid computing two uninteresting TRs consisting in: the last three instances of the motif \( ACG ACG ACG \), and the last two instances \( ACG ACG \). A tandem beginning with the motif AGC, instead, needs to be searched since it could be the starting point of a second TR not entirely included in the first result (in the case of the example \( ACG ACG ACG ACG ACG AGT AGT \)).

A second class of artifacts is that of pairs (or groups) of overlapping results consisting in the same TR (with the same motif length and copy number) shifted one position forward along the sequence (namely starting and ending positions differ by only 1 bp). This case arises only when the initial characters of the TR match the corresponding characters immediately after the TR. Dealing with this class of artifacts, the searching procedure attempts to expand a retrieved TR allowing it to have a final (fractional) pure motif (see lines 22–25 of Algorithm 1). The resulting extended TR is conceptually equivalent to merging together a sequence of shifted TRs into a longer result. The above equivalence suggests a sufficient condition to determine whether searching from a given position would lead to find an artifact. In fact, since a TR with a \( 0 < l < \ell \) long final motif is equivalent to a sequence of \( \ell \) TRs in which motifs are shifted by 1 bp, all the positions at distance at most \( l \) from a marked element in the bit vector must be the starting coordinates of a sub-TR of the expanded one. As a result, these positions can be ignored.

A last class of artifacts derives from the fact that the same TR can admit several distinct combinations of period length and copy number. Since Dot2dot increasingly tests several possible motif lengths (see line 2 of Algorithm 1), the absence of a specific mechanism to filter (or to avoid the computation of) all the possible combinations of the same result would lead to a potentially huge redundancy in the output. Dealing with impure TRs the only available option is that of computing all the combinations and then evaluating which one better fits a pre-determined criterion (in our case we prioritize the pure one). Pure TRs, instead, do not require computing all the possible combination. In fact, testing for multiples of the motif length can only produce either TRs of the same size or shorter. Consequently, once we find a pure TR we do not need to test multiples of its motif length.

3 Results

We experimentally tested our software to assess whether it is able to find non-naive biologically relevant TRs. Moreover, we thoroughly scanned the literature to find the widest possible pool of alternative algorithms to compare with. As a testing dataset we used five collections of TRs: 45 disease-related TRs, the 20 extended CODIS repeats, a set of Y-STR loci, 620 markers from the Marshfield panel and a wide list of TRs located in the regulatory regions. Although it could be considered inconsequential for our purposes, we choose to map all TRs and genes onto the most recent main release of the human genome (namely hg38). We manually mapped genes querying the UCSC genome browser (https://genome-euro.ucsc.edu) while we used the batch LiftOver interface (https://genome.ucsc.edu/cgi-bin/hgLiftOver) to convert the coordinates of TRs. Results show that our method is able to find biologically relevant repeats not reported from the other methods.

3.1 Tandem repeats discovery tools selection

Despite the vast literature on TRs discovery tools [see Lim et al. (2013) for a recent survey], only few algorithms are usable in practice. In fact, most tools seem to be no longer available or no longer supported (Abajian, 1994; Krishnan and Tang, 2004; Kurtz et al., 2001; Parisi et al., 2003; Pokrzywa and Polanski, 2010; Sokol et al., 2007; Taneda, 2004; Wirawan et al., 2010; Zhou et al., 2009); some other is still available but no longer maintained [this is the case e.g. Wexler et al. (2005)] that is distributed only in binary form and requires an obsolete version of the operating system). Some algorithms are subjected to limitations that make comparing with them unfair. In particular: STAR (Delgrange and Rivals, 2004) uses a dictionary-based approach that makes its computational cost unaffordable even using a small dictionary; MsDetector (Girgis and Sheetlin, 2013) and IMEx (Mudumbai and Nagarajaram, 2007) are designed only for microsatellites with motif length \( \leq 6 \); the approach in Thiel et al. (2003) leverages on a species-specific database; E-TRA (Karaca et al., 2005) can only find perfect TRs; and Pop (2015) provides only a visual representation of the distribution of TRs over the input sequence.

At the end of our investigation we identified only seven algorithms that can be realistically employed in daily TR discovery tasks: tandem repeats finder (TRF) (Benson, 1999), mreps (Kolpakov et al., 2003), tandemSWAN (Boeva et al., 2006), TRStalker (Pellegrini et al., 2010), SciRoKo (Koefler et al., 2007), TROLL (Castello et al., 2002) and RepeatMasker (Smit et al., 2017) (http://www.repeatmasker.org). Since all these methods are provided with a default set of parameters that perform well in most cases, after verifying that they match the characteristics of our datasets, we always used them (see details in the Supplementary Material).

3.2 Disease-associated tandem repeats

Due to the proven relationship between repeat expansion and a consistent number of neurological and neuromuscular disorders
3.3 DNA profiling tandem repeats

As a consequence of their contribution to DNA profiling in forensic sciences, a large database of short TRs [STRbase Ruitberg et al. (2001)] has been made publicly available on the web (http://www. cslt.nist.gov/strbase/). Although STRbase does not report the exact genomic location of the censused STRs, it provides useful information that we exploited to pinpoint the coordinates of the two most commonly used collections of TR listed in it: CODIS and Y-STR.

3.3.1 FBI CODIS

The Combined DNA Index System (CODIS) database consists of 13 tetra-nucleotide TRs spread in 12 chromosomes. As of January 1, 2017 this dataset has been extended with 7 new tetra-nucleotide TRs: D1S1656, D2S441, D2S1338, D10S1248, D12S391, D19S433 and D22S1045. We collected the coordinates in hg19 of the 13 CODIS core STR loci from the lQbSTR (Gymrek et al., 2012) website, while we manually retrieved the coordinates of the new TRs.

3.3.2 Y-STR

Y-STR is a collection of short TRs in the Y chromosome with period lower than 6 and size ranging from 24 to 166 bp. These repeats are often used for paternity or genealogical tests as well as for forensic purposes. An almost complete list of these loci has been published in Gymrek et al. (2013) and the genomic coordinates in hg19 are available in the lQbSTR website. The two markers DYS448 and DYS449 are not TRs in a strict sense and consist of two pure STRs interrupted by a small spurious sequence. According to Gymrek et al. (2013), for these markers we included both: the entire STR and the two parts. We completed our list including two extra TRs not mentioned in Gymrek et al. (2013) but present in the lQbSTR website: DYS640 and DYS464. The forensic value of DYS464 is studied in Butler and Schoske (2004). The final collection of Y-STR consists of 86 loci.

3.4 Marshfield linkage panel

The Marshfield linkage panel (Rosenberg et al., 2005) consists of more than 600 loci distributed across the autosomes each of which containing a short and highly polymorphic TR. The main purpose of this panel is that of exploiting the great degree of polymorphism of TRs to conduct genome-wide population analyses. The original work in Rosenberg et al. (2005) neither describes in details the structure of the TRs nor reports their coordinates. Thus, some authors used TRF to pinpoint the repetitive structures. This choice is sensible for certain problems [e.g. in Willems et al. (2017) where the Marshfield panel is used as a benchmark for genotyping], but it is inappropriate for our purposes. In the Supplementary Material of Pemberton et al. (2009), the authors provide the PCR primers, the Refseq sequences, as well as a manually curated description of the TR structures, for 627 of the Marshfield loci (see the file Pemberton_AdditionalFile1_11242009.txt in the Rosenberg’s website https://web.stanford.edu/group/rosenberglab/data/pembertonEtAl2009/). Using the Refseq sequences as input for blastn (http://blast.ncbi.nlm.nih.gov) we located 598 loci. We further obtained the hg38 coordinates of another 22 loci by means of the UCSC’s in silico PCR tool (https://genome. ucsd.edu/cgi-bin/hgPcr). Finally, we pinpointed the exact coordinates of each TR by a local alignment of the flanking regions of the TR in refseq and the locus in hg38. The resulting dataset consists in 620 microsatellites with size ranging from 8 to 270 bp.

3.5 Tandem repeats in the regulatory regions

Despite being ubiquitously distributed in eukaryotic genomes, TRs have been reported to be more abundantly present in regulatory regions and in particular in promoters (Sawaya et al., 2013; Vinces et al., 2009). Their great variability as well as intrinsic instability suggests that mutations of this class of genotypic variation in the promoter regions can influence the observed phenotype (Gemayel et al., 2010). Notwithstanding their importance, a manually curated reference database of variable TRs in promoter regions is not available yet. Partial lists of pure TRs are reported in Heidari et al. (2012) and Ohadi et al. (2012) while in Bolton et al. (2013) the authors describe a resource where a partial list is obtained by means of the only TRF software. Besides the database resource, the authors of Bolton et al. (2013) provide a description of a sensible
methodology that we used to recompute the list of TRs in the promoter regions using all the algorithms available to us.

Following the procedure in Bolton et al. (2013) we downloaded the coordinates of the human genes from the UCSC table browser (Karolchik et al., 2004), then we removed non-coding and putative genes as well as genes not in haplotypic regions. After removing duplications we obtained a list of 36 096 elements including coding genes and isoforms. In order to ensure that the promoter regions have been entirely covered, as an input sequences we used a 3 kb interval from −2 kb to +1 kb from the transcription start sites. We run all the algorithms on these sequences limiting the TR period up to 9 bps, discarding results with purity lower than 90% and removing TRs shorter than 23 bp. Given the reasonably limited number of results, we could refine the list of TRs by: re-estimating the correct period length, and trimming spurious endpoints. Estimating the period length, we used a brute force procedure that tested all the possible combinations and decided for the shortest value maximizing purity. Then we compared the first and the last instance of each TR motif with the corresponding consensus sequence and trimmed those not matching. Finally, we get rid of overlapping TRs by means of an iterative procedure that, at each step, removed the less pure overlapping TR or, in case of tie, the overlapping TR with higher motif length or the shortest one. At the end of this procedure we obtained a final list of 15 326 TRs.

3.6 Evaluation metrics
Assessing quality of TR discovery algorithms via comparing results with a gold standard requires a few caveats. A first issue is the definition of matching. In the most restrictive setting, one could be interested in the exact match of the starting and ending coordinates, while in general a limited degree of divergence is acceptable. A perfect match is very hard to achieve and it could not be significant because of the subjectivity of the identification procedure. In fact, the coordinates of (more often impure) TRs can slightly differ according to the interpretation given by the curator during the manual annotation phase. In addition, when a TR is adjacent to a region similar enough to the repeat, the overlap given by the curator during the manual annotation phase. In addition, when a TR is adjacent to a region similar enough to the repeat itself, many alternatives are equally possible. In this case, establishing which is the ‘correct’ repeat, results in an arbitrary choice.

Another relevant issue is that of redundancy (namely, the presence in the output of overlapping TRs). Despite often due to software artifacts, a moderately redundant output may not be problematic when the subsequent analysis is automated, while it could defeat the purpose of an algorithm when only a restricted number of results can be analyzed. An evaluation based only on the score of the best hit can penalize those algorithms that employ filtering to reduce the number of biologically irrelevant results.

Finally, the possibility of defining the concepts of true/false positives/negatives, that are at the base of measures like sensitivity and specificity, should be critically examined. As observed in Saha et al. (2008), evaluating an ab-initio method through a gold standard dataset (either the output of another algorithm or a collection of TRs) the true positives are easily defined as the algorithm results that are also listed in the gold standard, while the false negatives are sequences of the testing dataset not reported in the list of results. The problem arises with the other two classes. In particular, it is questionable whether a result reported by the tool but not present in the reference dataset is a false positive or it is a new legal TR that was not previously known. The difficulty of defining the concepts of false positives and true negatives has the effect of hindering the estimation of specificity. Sensitivity, instead, can be computed through the standard formula. However, since sensitivity and specificity are dual evaluation functions that need to be considered as a whole, we decided to use alternative measures. In particular, we used precision and recall.

In order to address the issue of matching algorithm results with the gold standard, we used the Jaccard coefficient. This score has originally been employed to measure the degree of similarity between sets. Subsequently, it has been extended to measure the overlap between intervals. In short, the Jaccard coefficient is defined as the ratio of the length of the intersection of two intervals divided by the size of their union. Its value is bounded in the range [0, 1] and to a higher value corresponds a higher degree of matching. Entirely covering a TR is necessary but not sufficient to get the highest score, in fact, the Jaccard coefficient has value 1 only when the comparing intervals have exactly the same coordinates.

Dealing with redundancy, we used three measures: the average number of results covering an element of the gold standard, the average precision and the average recall. Let \( T = \{ t_1, \ldots, t_n \} \) be a dataset of TRs, \( R \) be the set of results of a given algorithm, and \( R(t_i) \) be the subset of \( R \) overlapping with \( t_i \) by at least 1 bp. We further denote \( jac(x) \) as the Jaccard coefficient between two genomic intervals. The average precision and average recall are defined as follows:

\[
\sigma_P(T, R) = \frac{1}{n} \sum_{i=1}^{n} \frac{\sum_{x \in R(t_i)} jac(x, t_i)}{|R(t_i)|}
\]

\[
\sigma_R(T, R) = \frac{1}{n} \sum_{i=1}^{n} \max_{x \in R(t_i)} jac(x, t_i)
\]

The above measures have several advantages. Firstly, they are independent from the arbitrary choice of a threshold value. Secondly, results over different datasets can be merged into a single score or can be compared directly. Lastly, it is possible to compare algorithms that apply filtering with methods that do not use it. In fact, even in a case where the filtering phase removes the most overlapping repeat, causing the Jaccard score of the second best hit to drop under threshold, the removal of a promising repeat could be balanced by the removal of a certain number of irrelevant repeats with low Jaccard score.

4 Discussion
In this section we discuss the outcome of our comparative evaluation. We run Dot2dot using two sets of parameters: one with the default values but without any filtering, and one with the same values but enabling the most stringent filtering (see Supplementary Material for details). TRStalker was run in multiprocessor mode using 64 threads. We also set a time limit of four days to accomplish the input length due to the computational cost of TRStalker, we run this software also on trimmed subsequences of length at most 10 kb centered on a TR (notice that this had no effect on the TRs in the regulatory regions since the input is always shorter). Although a direct comparison of TRStalker on the diseases and CODIS datasets with or without shortened input reveals a remarkable advantage in favor of the former (henceforth indicated asTRStalker*), using trimmed input was the only way to estimate TRStalker performance on all the datasets.

Table 1 reports the number of TR identified setting Jaccard score to 0.5 and 0.7 (see results for other thresholds in the Supplementary Material), the average number of results per locus (RPL), the average precision and the average recall of each algorithm for the five test collections. Accepting Jaccard =0.5 Dot2dot and TRStalker* rank alternatively first and second in terms of absolute number of
located TRs with a negligible gap. TRStalker on the diseases loses only two TRs, while the other algorithm in general misses a remarkable number of elements. Increasing Jaccard to 0.7 causes Dot2dot to become less accurate than TRStalker and TRStalker* but still more accurate than the others. This higher accuracy, however, is the effect of a very large redundancy due to the exhaustive enumeration of all the possible alternative TRs covering the same locus. In fact, TRStalker and TRStalker cover a locus with an average of over 110 different results.

Although the ability of identifying the repeats of the gold standard with a reasonably high Jaccard score is a desirable property, achieving a high recall at the cost of a large output redundancy can greatly reduce the usefulness of an algorithm in practice. In particular, a good filtering strategy should increase the average precision at the cost of a negligible reduction of accuracy.

Table 1 shows that an aggressive filtering typically has a positive impact on the average precision as well as on controlling the redundancy of the output. In fact, the algorithms implementing the most aggressive filtering strategy (Dot2dot-Filter, TRF and SciRoKo) achieve the highest values of average precision. As a notable exception, the (embedded) purity-based filtering of TandemSWAN caused the algorithm to filter out most of the TRs on the profiling datasets because they were considered uninteresting. A high level of redundancy is not necessarily a guarantee of a high average recall. This is the case, e.g. of Troll that has the third highest number of RPL but achieves one of the lowest average recall. Dot2dot, TRStalker and TRStalker*, which have the most verbose output, achieve the highest average recall. However, in spite of having comparable average recall (almost the same narrowing to TRStalker), Dot2dot returns a number of RPL of the same order of magnitude of the other methods, while TRStalker produces two orders of magnitude more RPL.

Comparing Dot2dot run with and without filtering, we observed how our filtering strategy has a remarkably positive impact in terms of a drastic reduction of overlapping results, passing from about 5 RPL to ~1. Filtering causes an increase of average precision of about 0.15 allowing Dot2dot to attain the highest score over all the tested datasets at the cost of a limited reduction of average recall (~0.06). However, this lower recall does not change the relative ranking of our algorithm in comparison with the other methods.

### 4.1 Running time

Although running time is a secondary feature for TRs discovery algorithms, it can still be important to evaluate the feasibility of large-scale analyses of whole-genomes and NGS data. Assessing the selected algorithms on whole-genomes, we run them on seven assembled references with sizes ranging between 1.3 and 27 Mbp, available on the NCBI website. NGS data, instead, have been tested on the high-coverage long reads of the NA12878 individual sequenced with Oxford Nanopore Technology (Jain et al., 2018). However, since Dot2dot and TRF are the sole two methods that can directly handle large multifasta files (Mreps, Tandem SWAN can handle only one sequence at a time, Troll and SciRoKo, instead, require one file for each sequence to be specified in the command line). We narrowed comparison on NGS data only to them.

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**Table 1.** Average precision \( \sigma_p \), average recall \( \sigma_R \), average number of reported results covering a target locus (RPL) and total number of TRs intersected (with Jaccard = 0.5 and Jaccard = 0.7) of the compared algorithms and datasets.

| Dataset   | Measure | Dot2dot-filter | Dot2dot | TRF | MREPS | TRStalker | TRStalker* | SWAN | Troll | SciRoKo | Repeatmasker |
|-----------|---------|----------------|---------|-----|-------|-----------|------------|------|-------|---------|--------------|
| Diseases  | \( \sigma_p \) | 0.830 | 0.678 | 0.722 | 0.630 | 0.464 | 0.491 | 0.372 | 0.508 | 0.724 | 0.452 |
|           | \( \sigma_R \)  | 0.835 | 0.899 | 0.763 | 0.686 | 0.901 | 0.960 | 0.575 | 0.571 | 0.752 | 0.475 |
|           | RPL       | 1.0 | 6.0 | 1.4 | 1.5 | 155.9 | 157.5 | 2.0 | 4.1 | 1.1 | 1.2 |
|           | \#TR \( j = 0.5 \) | 44 | 45 | 37 | 37 | 43 | 45 | 27 | 29 | 38 | 24 |
|           | \#TR \( j = 0.7 \) | 36 | 42 | 33 | 23 | 43 | 45 | 24 | 18 | 33 | 20 |
| CODIS     | \( \sigma_p \)  | 0.860 | 0.721 | 0.836 | 0.659 | 0.485 | 0.565 | 0.682 | 0.819 | 0.812 |
|           | \( \sigma_R \)  | 0.860 | 0.899 | 0.850 | 0.818 | 0.839 | 0.988 | 0.797 | 0.867 | 0.822 |
|           | RPL       | 1.0 | 6.3 | 1.1 | 2.1 | 188.2 | 172.2 | 0.0 | 3.2 | 1.2 | 1.0 |
|           | \#TR \( j = 0.5 \) | 19 | 19 | 20 | 20 | 18 | 20 | 0 | 19 | 20 | 19 |
|           | \#TR \( j = 0.7 \) | 18 | 18 | 15 | 15 | 18 | 20 | 0 | 16 | 16 | 15 |
| Y-STR     | \( \sigma_p \)  | 0.877 | 0.706 | 0.770 | 0.617 | — | 0.535 | 0.021 | 0.682 | 0.827 | 0.721 |
|           | \( \sigma_R \)  | 0.879 | 0.916 | 0.786 | 0.712 | — | 0.979 | 0.029 | 0.777 | 0.841 | 0.729 |
|           | RPL       | 1.0 | 6.1 | 1.1 | 2.1 | — | 205.5 | 2.5 | 2.8 | 1.1 | 1.0 |
|           | \#TR \( j = 0.5 \) | 86 | 86 | 70 | 74 | — | 86 | 3 | 79 | 80 | 67 |
|           | \#TR \( j = 0.7 \) | 74 | 81 | 65 | 59 | — | 86 | 1 | 75 | 69 | 62 |
| Marshall  | \( \sigma_p \)  | 0.856 | 0.637 | 0.784 | 0.662 | — | 0.559 | 0 | 0.683 | 0.810 | 0.767 |
|           | \( \sigma_R \)  | 0.860 | 0.905 | 0.794 | 0.755 | — | 0.975 | 0 | 0.792 | 0.830 | 0.775 |
|           | RPL       | 1.0 | 7.1 | 1.1 | 2.0 | — | 154.3 | 0.0 | 3.2 | 1.1 | 1.0 |
|           | \#TR \( j = 0.5 \) | 589 | 609 | 559 | 577 | — | 619 | 0 | 583 | 587 | 554 |
|           | \#TR \( j = 0.7 \) | 503 | 557 | 447 | 405 | — | 619 | 0 | 490 | 471 | 437 |
| Promoters | \( \sigma_p \)  | 0.825 | 0.667 | 0.663 | 0.575 | 0.422 | 0.422 | 0.663 | 0.517 | 0.808 | 0.743 |
|           | \( \sigma_R \)  | 0.803 | 0.934 | 0.548 | 0.687 | 0.929 | 0.929 | 0.447 | 0.627 | 0.709 | 0.432 |
|           | RPL       | 1.0 | 4.8 | 1.4 | 1.9 | 116.0 | 116.0 | 2.2 | 2.1 | 1.0 | 0.6 |
|           | \#TR \( j = 0.5 \) | 13783 | 15192 | 8864 | 12490 | 15264 | 15264 | 5156 | 10939 | 12125 | 7128 |
|           | \#TR \( j = 0.7 \) | 12329 | 14792 | 7903 | 7880 | 15098 | 15098 | 3233 | 5723 | 10492 | 6286 |

Note: TRStalker run on the trimmed sequences is reported as TRStalker*. (The best value is highlighted in bold.)
We used a MacOS-based workstation endowed with a processor Intel Xeon 3.1GHz and run the software in single thread mode. For tandemSWAN and Troll, which run only under Linux, we had to use a different hardware. We computed the performance difference between the two machines by comparing the speed of Dot2dot over chromosome 1 of hg38. We found that the Linux server is 1.4556 times faster. As a result, we used this constant to adjust tandemSWAN and Troll’s running time.

We report in Table 2 the running time of the tested algorithms. We excluded TRStalker because it cannot run on large sequences and Repeat Masker because its running time is dominated by the identification of other classes of repetitions different from TRs. Since we endorse filtering, we run Dot2dot only with it. We notice that this choice does not give Dot2dot any advantage in the comparison, in fact, without filtering our software would run slightly faster.

As Table 2 shows, three algorithms are unable to run on the majority of the genomes. This is mostly due to intrinsic thresholds hardwired in the software. In particular, Mreps has a constraint on the length of the longest consecutive stretch of Ns in a sequence, which would be the second fastest software, has a limit of the genome’s length with a small stable constant factor.

Table 2. Running time of the compared algorithms over seven common reference genomes

| Organism name      | Size Mb | Dot-to-dot filter | TRF       | Mreps     | Tandem SWAN | SciRoKo   | Troll     |
|--------------------|---------|-------------------|-----------|-----------|-------------|-----------|-----------|
| Pinus lambertiana  | 2760.70 | 12 h 15 min 18 s  | 16 h 15 min 14 s | N/A       | N/A         | 2 h 13 min 51 s | N/A       |
| Triticum aestivum  | 13427.40| 5 h 57 min 14 s  | 11 h 13 min 43 s | N/A       | N/A         | 41 min 59 s   | N/A       |
| Locusta migratoria | 5759.80 | 2 h 37 min 14 s  | 2 h 25 min 12 s | N/A       | N/A         | 18 min 59 s   | N/A       |
| Homo sapiens       | 3241.95 | 1h 24 min 15 s   | 2 h 40 min 51 s | 12 h 20 min 14 s | N/A         | 10 min 43 s   | 35 min 14 s |
| Rattus norvegicus  | 2870.18 | 1 h 18 min 52 s  | 2 h 04 min 44 s | N/A       | N/A         | 9 min 40 s    | N/A       |
| Mus musculus       | 2807.72 | 1 h 16 min 29 s  | 1 h 55 min 37 s | N/A       | N/A         | 9 min 41 s    | N/A       |
| Danio rerio        | 1371.72 | 36 min 29 s      | 2 h 33 min 36 s | 2 h 07 min 54 s | 13 h 59 min 40 s | 5 min 7 s | 17 min 16 s |
| NA12878            | 82705.67| 1 d 12 h 15 min 18 s | 1 d 16 h 15 min 14 s | —         | —           | —         | —         |

Note: The genome dimension is measured as the size in Mb of the corresponding fasta file.

5 Conclusion

In this paper we presented Dot2dot: a new algorithm for TR identification in a target genome. Our model of repeat has shown to be general enough to capture well various classes of TRs with different characteristics: pathology-linked, forensic, for population analysis, genealogic-oriented and repeats in the regulatory regions. Experiments have shown that Dot2dot is fast and effective since it was able to identify almost all the TRs of our test collections with an accuracy of at least 0.7 in terms of Jaccard score. Even applying a severely stringent filtering where overlap among the returned repeats is not allowed, our algorithm is still more accurate than the alternative tested tools. Tests over the entire human genome have confirmed the hypothesis that the longest TR (with a length of 2495 bp) is several order of magnitude shorter than any of the input sequences enabling Dot2dot to run in linear time with the input length.

Dot2dot is freely available and can be used without restrictions. To make it useful in the daily laboratory practice we enabled it to read standard formats for both assembled genomes (fasta) and NGS data (fastq) as well as return its output also in a standard bed format.

Another contribution of this paper is that of proposing a rigorous assessment methodology of TRs discovery algorithms as well as providing five reference collections of TRs (four of which manually curated). We hope that the proposed methodology and datasets can help to facilitate future research in this field.

Funding

This work was supported by the project ‘RepeatALS’ FGR8 17/2013 funded by Arisla (Italian Society for Research on Amyotrophic Lateral Sclerosis) and the project PRIN 201534HNXC. The role of tandem repeats in neurodegenerative diseases: a genomic and proteomic approach funded by the Italian Ministry of Education and University (MIUR).

Conflict of Interest: none declared.

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