Quantifying the Risk of Wildfire Ignition by Power Lines under Extreme Weather Conditions

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Abstract—Utilities in California conduct Public Safety Power Shut-offs (PSPSs) to eliminate the elevated chances of wildfire ignitions caused by power lines during extreme weather conditions. We propose Wildfire Risk Aware operation planning Problem (WRAP), which enables system operators to pinpoint the segments of the network that should be de-energized. Sustained wind and wind gust can lead to conductor clashing, which could ignite surrounding vegetation. The 3D non-linear vibration equations of power lines are employed to generate a dataset that considers physical, structural, and meteorological parameters. With the help of machine learning techniques, a surrogate model is obtained which quantifies the risk of wildfire ignition by individual power lines under extreme weather conditions. The cases illustrate the superior performance of WRAP under extreme weather conditions in mitigating wildfire risk and serving customers compared to the naïve PSPS approach and another method in the literature. Cases are also designated to sensitivity analysis of WRAP to critical load-serving control parameters in different weather conditions. Finally, a discussion is provided to explore our wildfire risk monetization approach and its implications for WRAP decisions.

Index Terms—wildfire, power system resilience, risk quantification, surrogate models, weather conditions.

I. INTRODUCTION

A. Motivation

WILDFIRES are among the threats that could potentially lead to disastrous events worldwide. Arguably, fire seasons are getting longer and more frequent, primarily due to climate change and global warming [1]. The wildfire frequency and the burned area in the western U.S. have grown exponentially since 1950 [2]. The causes of wildfire ignition include natural sources (lightning), human activities (arson, campfire, etc.), equipment faults, and power lines, among other things [3]. Pacific Gas & Electric Company (PG&E) declared 414 fire ignition events during 2015-2017 caused by electric power lines [4]. According to the historical data during the period 1960-2009 in Southern California, fires ignited by power lines burn on average ten times the area burnt as a result of fires initiated by other sources [5]. Extreme winds, such as the ones occurring during the fall season in Southern California, not only increase the risk of power line-related ignitions but also facilitate the propagation of fire. Reportedly, wildfires caused by power lines account for almost half of the most destructive fires in California history [6]. Conductor clashing (phase to phase faults), fall of the line on the ground (phase to ground faults), arcs, and contact with the surrounding vegetation are among the incidents related to power lines that could cause ignitions [7].

In addition to the wind, temperature, humidity, and vegetation are among the meteorological and geographical factors correlated with the chances of fire ignitions by power lines [8], with the wind as the leading factor. Although low wind speeds will cool off conductors and can benefit dynamic line rating [9], high wind speeds can lead to faults within power lines. According to the analysis of the 11-year outage record data provided by San Diego Gas & Electric (SDG&E), for every 25 km/h increase in the wind gust speed, the outage probability is increased ten times [5]. That is one reason why higher wind speeds are associated with higher chances of wildfire ignition.

High sustained wind speeds (average wind speed lasting over 10 minutes) typically occur during California's late summer and fall seasons. Wind gusts could significantly affect the swing angle of the conductors [10]. The combination of high sustained wind speeds and wind gusts could lead to conductor clashing, which, together with hot and dry weather conditions, dramatically increases the risk of wildfires taking place. The clashing of the energized power line conductors may cause vaporization and melting of the conductor materials and ejection of the molten metal as small particles [11]. Drop of hot particles due to conductor clashing on dried vegetation or direct contact between conductors and vegetation can potentially ignite wildfires [12]. That is why utilities across California adopted Public Safety Power Shut-offs (PSPS) to avoid such ignitions under extreme conditions with wind gusts exceeding 22.8 m/s.

The California Public Utilities Commission allows utilities to deliberately cut off power to electrical lines as a preventive measure in high-risk situations with a looming threat of wildfire ignition [6]. From 2013 to 2020, PG&E, SDG&E, Southern California Edison, and PacifiCorp collectively performed 51 PSPS events in multiple locations within California, which impacted 3.2 million customers [13]. However, a PSPS event has its own risks and unfavorable consequences, particularly for medically vulnerable populations and low-income communities [8]. In October 2019, power shut-offs by PG&E affected 1.8 million customers, with outages lasting more than five days in some cases. PSPS events cost the California economy in the order of billion dollars [14], while a lack of power supply could lead
to casualties [15]. It can be concluded that although PSPS schedules are a practical approach to proactively mitigating wildfire risk, they could impose unnecessary difficulties if blanket outages are conducted throughout a power grid within a region. In this work, we propose a method that can pinpoint the network segments with a higher fire ignition risk, which could help PSPS events be targeted towards those lines of the grid instead of an entire section of the grid.

Although several meteorological phenomena could influence wildfire ignition risk, this study focuses on high wind speed and gust conditions. This choice is mainly because the impact of wind speed on power lines’ displacement can be modeled and explained by power line motion equations, allowing for a scientific analysis of windy conditions. Additionally, from the practical point of view, PSPS events are scheduled based on extreme wind speed conditions/predictions rather than other factors. Throughout this paper, extreme weather situations denote conditions with high wind speeds. We also limit this study to modeling conductor clashing rather than other sources of wildfire ignition inside a power system, such as phase to ground faults and contact with the surrounding vegetation, given conductor clashing is the only cause modeled in a generalized approach. Currently, no models account for other ignition causes inside a power system.

With the increase in the availability of meteorological sensing data and estimation techniques with high granularity, this paper presents a scientific setup for reflecting the impact of wildfire ignition risk induced by strong winds on the power system operation. To this end, we introduce a machine learning-based surrogate model that can instantly quantify the risk of wildfire ignition for each line of the grid. The surrogate model predicts and assigns scores that represent the conductor-clashing probability of a power line based on real-time wind speed data. The procured quantified measure will pave the way to incorporate wildfire risk assessment into operational planning models within grids at the risk of wildfire. We introduce the Wildfire Risk Aware operation planning Problem (WRAP), which integrates the generated wildfire risk scores into the power system operation. The resulting model can be used to determine precisely which sections and lines of the grid should be subject to PSPS, thereby minimizing the area and population impacted by unnecessary outages while taking the potentially disastrous impacts of extreme winds into consideration.

B. Literature Review

Extensive research has been dedicated to the assessment and mapping of wildfire ignition risk within different regions of the world. A fire occurrence prediction model is presented in [16] for the northeast regions of China, where wildfire probabilities are obtained from ten variables such as altitude, slope, and distance to structures. In [17], eight factors are integrated into a regression model to model wildfire ignition risk in Portugal. These studies tend to predict the wildfire risk regardless of the ignition cause and focus on historical data. As a result, various overlays have been developed through the Geographic Information System (GIS). Several researchers in the field of power systems have proposed wildfire risk assessment models with the help of these tools. Authors in [18] propose a method for the selection of power lines that should be modified to mitigate wildfire ignition risk, but no model is considered for the operation of the electricity network. A similar approach based on the spatio-temporal probability of wildfire ignition within a power system is utilized in [19]. Other methods for wildfire risk assessment within power lines according to historical and geographical data are proposed in [20], where estimation functions such as logistic regressions [21], and Bayes network [22] are utilized. However, wildfire risk values used in these works are obtained through GIS overlays based on historical data and location, rather than ignitions induced by power lines.

A review of electricity grid vulnerabilities amid natural disasters, including wildfires, is presented in [23]. A resilient mitigation strategy for the short-term operational planning of a power system during wildfires considering the thermal effects of wildfires on the dynamic line rating is given in [24]. The authors in [7] have proposed a learning-based algorithm for early detection of wildfire ignitions due to high impedance faults. An overview of wildfire risk mitigation plans such as PSPS schedules is presented in [25], and several risk management strategies, which are carried out by utilities, are explored. An optimization framework to balance the wildfire risk and power shut-offs is presented in [26]. Wildfire risk in this work is solely based on the energization status of components in the electricity grid; the impact of other factors, such as weather conditions, is not incorporated. The authors in [27] developed a fire hazard prevention system based on meteorological factors, including extreme wind speed. However, it is not clear how the data is modeled to forecast hazards, and no model is proposed to reflect wildfire risk in the scope of preventive measures. The probability of wildfire ignition due to line fault and arc ignition is computed in [28], and the effect of wind is also explained. However, no model is proposed to incorporate the resulting risk values into power system operation. An overview of the recent trends in the relevant literature is displayed in Table I.

| Reference | Power system model | Model ignition by lines | Model weather conditions | Integrated risk optimization |
|-----------|--------------------|-------------------------|--------------------------|------------------------------|
| [7]       | ✓                  | ✓                       | ✓                        | -                            |
| [18], [20], [22], [21] | -               | -                       | ✓                        | -                            |
| [19], [27] | ✓                | ✓                       | ✓                        | -                            |
| [24]      | ✓                  | ✓                       | ✓                        | -                            |
| [28]      | ✓                  | ✓                       | ✓                        | -                            |
| [26]      | ✓                  | ✓                       | -                        | ✓                            |
| This work | ✓                  | ✓                       | ✓                        | ✓                            |

It is noticed in Table I that no work in the literature has proposed a model that incorporates the wildfire ignition risk of power lines into the system’s operation planning. The only exception is reference [26] where a risk model is integrated into the operation problem. However, the authors obtain relative risk scores rather than using a physical model,
and the impacts of weather conditions are neglected. As suggested in a review article on wildfire risk management in power grids [29], there is a lack of research on wildfire prediction when power grid infrastructures could potentially cause the fire. A gap in assessing the impact of meteorological conditions on power lines using a physical model and building a scoring mechanism to quantify the probability of conductors clashing exists in the literature. This paper aims to fill this gap by presenting a surrogate model that can efficiently quantify the risk of wildfire ignition under extreme weather conditions considering the wind speed, wind gust, wind direction, and the structure of the power lines, including span, conductor diameter, and phase clearance.

C. Summary of the Contributions

The contributions of this paper are outlined as follows:

1) A method for quantifying the risk of power line conductor clashing under extreme wind conditions is presented based on a physical model. We introduce a scoring method to determine the extent to which each conductor is clashing with nearby conductors. The predicted score ranges between 0 and 1, where 0 means no clashing is happening, while 1 means the whole conductor is under clashing. This high-granularity scoring system provides a well-quantified risk of wildfire for each individual power line. The resulting wildfire risk creates a scientific foundation to quantify the risk of the operation of each specific power line during specific extreme weather conditions.

2) A comparison of different learning algorithms for predicting the risk of wildfire is performed, and the most accurate model is proposed to predict the conductor-clashing score. The final choice is compared and verified against the nonlinear motion model, and presents a desirable performance which allows it to be confidently utilized as a surrogate model for the original nonlinear equations.

3) We present WRAP to incorporate the quantified wildfire hazard risk into power system operation. No study has proposed a planning model which is able to integrate the wildfire ignition risk with power system operation. With the availability of the required meteorological data predictions, WRAP supports decision-makers in deciding on the de-energizing of power lines for PSPS events and provides them with a mathematical foundation to study and analyze the impact of extreme weather conditions on wildfire risk.

II. Quantification of Wildfire Risk Score

In this section, the non-linear motion of power lines due to in-plane and out-of-plane vibrations is determined to evaluate the impact of wind on the motion of power lines, which is quantified as the conductor-clashing score. A dataset is generated that considers six physical and meteorological features to find the clashing score of each line. An advantage of the power line motion equations is their generality. This model is able to accurately predict power line position under any wind condition based on physics laws, as long as all the input data are provided. Consequently, the learning task does not need to be limited to real-world data. We can learn a general surrogate model by generating enough training and test datasets for the learning task.

A. Non-linear Equations for Motion of Power Lines

Here, the vibrational model that explains the movement of a power line under wind force is illustrated. Based on this model, we generated a training dataset that estimates the clashing score of a span within a power line. In-plane vibrations occur when a power line is in the plane and placed under gravity. Out-of-plane vibrations are perpendicular to the plane above. The spatial configuration of a power line is shown in Fig. 1, where \( P(x,t), P(y,t), \) and \( P(z,t) \) correspond to the components of external excitation along the \( x, y, \) and \( z \)-axes, respectively.

\[
\begin{align*}
\dot{q}_v(t) + a_2q_v(t) + a_3q_v^3(t) + a_4q_v^4(t) + a_5q_v^5(t) + a_6q_v^6(t) &= P_v \\
b_1\ddot{q}_\omega(t) + b_2q_\omega(t) + b_3q_\omega(t)q_\omega(t) + b_4q_\omega^2(t)q_\omega(t) + b_5q_\omega^3(t) + b_6q_\omega(t) &= P_\omega
\end{align*}
\]

Here, \( q_v \) and \( q_\omega \) respectively denote the generalized coordinates in \( x \)- and \( z \)-axes of a power line. The equations for acquiring the parameters \( a_1 - a_7, b_1 - b_6 \), and the initial conditions are given in [30].

B. Wind Effect on the Motion of Power Lines

A wind gust is a transient increase in the wind speed. It occurs when there is an abrupt change from high pressure to low pressure. It is ephemeral in nature and usually lasts for 20 seconds. The discrete wind gust is used to assess the conductors response to significant wind disturbances. The mathematical representation of a discrete wind gust is given in (2).

\[
V_{\text{wind}} = \begin{cases} 
V_m \left(1 - \cos\left(\frac{\pi x}{d_m}\right)\right) & 0 \leq x \leq d_m \\
V_m & x > d_m
\end{cases}
\]
Here, \( V_{\text{wind}} \) is the resultant wind velocity in the power line body axis frame, \( V_m \) is the wind gust amplitude, \( d_m \) is the length of gust, and \( x \) is the traveled distance. The gust length is the range over which the gust builds up, and the gust amplitude represents the increase in wind speed developed by the gust. The following assumptions are considered for the wind-induced vibrations of a power line.

1) The wind load acts in the out-of-plane direction of the power line. This is because the effect of wind load on power line weight is negligible.
2) The wind speed loading effect on the vibrations of power line is considered, but the aerodynamic effects are not considered. It is assumed that the wind load is considered constant and forces such as drag and lift are not modeled.

The external excitation due to wind in \( x \)-axis direction \( P(x, t) \) and \( z \)-axis direction \( P(z, t) \) are expressed in (3).

\[
P(x, t) = 0.5 \rho_a D_c C_D (v_{a-x} - \nu_c)^2 \quad (3a)
\]
\[
P(z, t) = 0.5 \rho_a D_c C_D (v_{a-z} - \omega_c)^2 \quad (3b)
\]

Here, \( \rho_a \) is the density of air, \( D_c \) represents power line width facing the wind, \( C_D \) represents power line shape factor, and \( v_{a-x} \) and \( v_{a-z} \) represent wind speed along the \( x \) and \( z \)-axes, respectively. The in-plane and out-of-plane power line vibrational velocities are represented by \( \nu_c \) and \( \omega_c \), respectively. Based on the above assumptions, the expressions for \( \alpha_7 \), \( b_6 \), \( P_c \), and \( P_w \) are updated considering the initial values of the state variables and the design hyper-parameters of the power line. The in-plane and out-of-plane responses of the power line using the Galerkin method [31] are represented by \( \nu_c(y, t) \) and \( \omega_c(y, t) \) respectively and are given in (4), where \( L_c \) denotes the span of the power line.

\[
\nu_c(y, t) = \sin \left( \frac{\pi y}{L_c} \right) \times q_\nu(t) \quad (4a)
\]
\[
\omega_c(y, t) = \sin \left( \frac{\pi y}{L_c} \right) \times q_\omega(t) \quad (4b)
\]

Consequently, a new solution is obtained for (1), which incorporates the impact of wind speed on power line motion.

C. Wildfire Risk Score Quantification

The first step in solving (1) is transforming it into a first-order differential equation through (5):

\[
Y_1 = q_\nu, \quad Y_2 = \dot{q}_\nu, \quad Y_3 = q_\omega, \quad Y_4 = \dot{q}_\omega \quad (5)
\]

Applying this transformation step turns (1) into a system of four first-order differential equations, which are solved by the Runge-Kutta method [32]. These methods are a group of numerical iterative techniques used to obtain the approximate solutions of ordinary differential equations. For example, consider the differential equation \( \dot{y} = f(x, y) \) with the initial condition \( y(x_0) = y_0 \). If this function is discretized with a granularity of \( h \), then applying the fourth-order Runge-Kutta method will result in an accumulative error in the order of \( O(h^5) \).

To obtain the wildfire ignition risk of power lines, we first segregate each line into several segments. Solving (1) in the presence of the wind-induced forces presented in (3) determines the spatial position of each segment of a line at any given time. We suppose two horizontally (vertically) adjacent lines will clash with each other if the value of \( q_\omega (q_\nu) \) becomes greater than a certain threshold, which is set based on the distance between two neighboring conductors. Solving the motion equations for all segments of a line will determine the ratio of the line segments that are clashing. As a result, a score ranging between 0 and 1 is obtained, which determines the extent to which a power line is in contact with the neighboring conductors.

D. Data Processing and Feature Importance Analysis

Different features and meteorological conditions such as the span of the power line, conductor diameter, phase clearance, wind speed, wind gust, and wind direction angle affect the wildfire risk score. We present a surrogate machine learning model that instantly returns a high-accuracy approximation of the risk value without solving the power line motion equations for several segments of a line. In order to find the surrogate model, first a training dataset is generated according to different ranges of features based on the practical characteristics of a power system. The total number of observations in the dataset is 435,600. Table II provides a sample of the generated dataset with scores calculated using the Runge-Kutta method. Data preprocessing comprises feature selection (dimensions of input data) and feature normalization (normalization of input data). Feature selection ensures that the power line features and meteorological conditions are contributing to predicting the score.

| Span (ft) | Conductor diameter (mm) | Wind speed (m/s) | Wind gust (m/s) | Phase clearance (ft) | Wind direction (°) | Score | ATASET GANPLETE GENERATED USING RUNGE-KUTTA METHOD |
|----------|-------------------------|-----------------|-----------------|----------------------|-------------------|-------|--------------------------------------------------|
| 600      | 33.03                   | 10              | 12              | 0.5                  | 45                | 0     | 0.12                                             |
| 800      | 34.02                   | 12              | 16              | 0.5                  | 180               | 0.01  |                                                  |
| 1000     | 31.05                   | 30              | 30              | 0.5                  | 90                | 0.12  |                                                  |

It is necessary to quantify the importance of input features to explore the potential improvement in the input data. The input feature importance of the random forest algorithm is given in Table III. For this analysis, Gini importance or Mean Decrease in Impurity (MDI) is used, which calculates the importance based on the number of times a feature is used to split a node. It is clear that wind speed and wind gust are among the important leading features, but it is also interesting to observe the impact of span on the clashing score. Although a single important feature cannot capture the thorough relationship between the input and output, it is rational to choose the significant features to predict the conductor-clashing score. Feature normalization is helpful when features of different ranges or scales exist.

It should be noted that the probability of power line conductors’ clashing could be also affected by the flow of the line. This is because the heating loss of electricity increases conductor temperature, which expands line sag and escalates
TABLE III

| Features                   | Importance (%) |
|----------------------------|----------------|
| Wind speed                 | 27.5           |
| Span of line               | 20.9           |
| Wind gust                  | 13.8           |
| Wind direction             | 13.5           |
| Conductor diameter         | 13.0           |
| Phase clearance            | 11.3           |

clashing probability. However, the results provided by [33] suggest that in extreme weather conditions, which are the focus of this work, heating loss is considerably mitigated by the cooling effect of wind. Hence, the impact of line current on clashing probability is neglected.

III. WILDFIRE RISK AWARE PROBLEM

This section presents WRAP, an operation planning problem that integrates the quantified risk scores into power system constraints. Applying WRAP to the operation planning of a power system subject to wildfire hazard ensures that the operational constraints of the power system are satisfied. WRAP enables the power system operator to avoid energizing high-risk lines under hazardous conditions. The proposed WRAP formulation is presented in (6), which illustrates how the procured wildfire risk quantification can be utilized in the operational planning problem of power systems.

\[
\text{min} \sum_{i,D} \left\{ \sum_{l \in L} K_i \cdot \psi_l^i \cdot I_l^i + \sum_{i \in I} K_d(P_{i,D}^t - P_{i,d}^t) \right\} \left( \sum_{s \in S} \sum_{g \in G} c_g^s P_g^t \right)
\]

subject to:

\[
\sum_{s \in S} P_{g,s}^t = P_g^t, \quad \forall g \in G, t \in T \tag{6a}
\]
\[
0 \leq P_{g,s}^t \leq P_{g,s}^T, \quad \forall g \in G, s \in S, t \in T \tag{6b}
\]
\[
0 \leq P_{g,s}^t + \sum_{g \in G_i} P_{g,s}^t \leq P_{g,\mathcal{L}^i}^t, \quad \forall g \in G, s \in S, t \in T \tag{6c}
\]
\[
P_g^t \leq P_{g,s}^T, \quad \forall g \in G, t \in T \tag{6d}
\]
\[
\alpha P_{i,D}^t \leq P_{i,d}^t \leq P_{i,D}^t, \quad \forall i \in I, t \in T \tag{6e}
\]
\[
-M(1 - I_l^1) + P_l^t \leq \frac{\theta_l^1 - \theta_l^2}{x_l} \leq P_l^t + M(1 - I_l^1), \quad \forall l \in L, t \in T \tag{6f}
\]
\[
-P_l^t \times I_l^1 \leq P_l^t \leq P_l^t \times I_l^1, \quad \forall l \in L, t \in T \tag{6g}
\]

The objective function is presented in (6a), where the summation of the conductor clashing scores, the value of load shedding, and the generation cost of units is minimized. The first term in the objective penalizes the wildfire risk associated with the energized lines by the monetization factor, $K_l$. The choice of this parameter and its implications are discussed in the case studies. Here, the quantified risk value of each line at each time is represented by $\psi_l^i$, where $I_l^i$ is a binary decision variable denoting the energization (if 1) or de-energization (if 0) status of each line at each time, $l$ is the index of lines in the set of power lines $\mathcal{L}$, and $t$ is the index of time in the set of time steps $\mathcal{T}$. In the second term of the objective, the operator is penalized by the penalty factor $K_d$ if load shedding takes place. Here, $P_{i,D}^t$ is the scheduled consumer demand, and $P_{i,d}^t$ is the amount of demand served at each bus at a given time, where $i$ is the index of buses in set $\mathcal{I}$. The last term in the objective function calculates the generation cost of units based on a piecewise linear function approximation. The output power of each generation unit at each time is divided into different segments denoted by $P_g^t$, where $c_g^s$ is the generation cost, $s$ is the index of segments in set $\mathcal{S}$, and $g$ is the index of generation units in set $\mathcal{G}$. The sum of power generation of each segment is equal to the total power generation of a unit, $P_g^T$, as shown in (6b). The power generation of each segment is constrained to its upper and lower bounds as presented in (6c).

The power flow balance at each node is given in (6d), where $P_g^t$ is the power flow of line $l$ at time $t$. The upper and lower limits of the power generation of each unit at each hour are constrained by (6e). The served demand at each bus is modeled in (6f), where $\alpha$ is a parameter ranging from 0 to 1 and assigns the ratio of the critical demand which must be served. The relationship between the power flow of each power line with the voltage angles of its connecting buses ($\theta_1^i, \theta_2^i$) and line reactance ($x_l$) is presented with two inequalities in (6g), where $M$ is an arbitrarily large number and $B_1^l, B_2^l$ are the sets of buses line $l$ is leading to and leaving from, respectively. The power line power flow capacity constraint is enforced in (6h), where the thermal capacity is presented by $P_l^t$. If a line is energized, i.e. $I_l^1 = 1$, the inequalities in (6h) become an equality constraint and the thermal limits in (6h) are applied. Conversely, if a line is de-energized (i.e., $I_l^1 = 0$), the power flow in the line will be zero.

The resulting WRAP formulation in (6) is a mixed-integer linear program, which can be solved via off-the-shelf solvers. The solution to WRAP will help system operators balance the risk of wildfire in the operation of the electricity grid under the risk of wildfire. By implementing the quantified risk values of each line at each time in the WRAP, the obtained scheduling of each line’s status and the output of generation units guides the system operator in decision-making under extreme weather conditions. Figure 2 illustrates the diagram of the proposed method, where the surrogate model feeds the underlying power line motion into the WRAP scheme to obtain the optimal PSPS schedule.

![Fig. 2. Flowchart of the proposed wildfire risk mitigation method](image313x112 to 558x221)

IV. SIMULATION RESULTS

In this section, the performances of different learning models are compared, and the results of the surrogate
model are verified through comparison with the original motion equation model. Next, the merits of WRAP are illustrated through comparison with two other approaches, namely naive PSPS and the method utilized by Rhodes [26]. The implications of the choice of $\alpha$ for WRAP are also investigated. Finally, a discussion is presented on wildfire cost monetization along with case studies.

A. Learning Performance

In this part, several aspects of the learning process for obtaining the surrogate model are investigated.

1) Comparison of Various Learning Algorithms: In order to learn a surrogate model, we performed a machine learning task using several well-known approximator structures. Here, the performance of each model is discussed and assessed with standard evaluation metrics. To demonstrate the merit of the proposed surrogate model, the best performing model is selected, and it is compared with the Runge-Kutta method. After careful hyper-parameter tuning, Random Forest Regression (RFR) displayed better performance than Multiple Linear Regression (MLR), Least Absolute Shrinkage and Selection Operator (LASSO), Support Vector Regression (SVR), and Deep Neural Network (DNN). The optimal performance metrics for each model are shown in Table IV.

| Measure                  | MLR | LASSO | SVR | RFR                  | DNN |
|--------------------------|-----|-------|-----|----------------------|-----|
| Mean Absolute Error (MAE)| 0.03| 0.03  | 0.02| 0.006 x 10^{-3}      | 0.2 x 10^{-3} |
| Relative MAE             | 0.96| 1.04  | 0.64| 0.16 x 10^{-3}       | 6.2 x 10^{-3} |
| Root Mean Square Error (RMSE) | 0.05| 0.05  | 0.04| 0.072 x 10^{-3}     | 0.6 x 10^{-3} |
| Relative RMSE with mean | 1.37| 1.52  | 1.24| 1.96 x 10^{-3}      | 10 x 10^{-3} |
| Relative RMSE with maxmin| 0.11| 0.12  | 0.10| 0.15 x 10^{-3}      | 1.3 x 10^{-3} |

The LASSO regression model is not performing better than MLR because all features are important for the learning process, and discarding a feature leads to poor performance. This is consistent with the feature importance analysis that deemed no input feature negligible. The non-linear SVR model based on the radial basis function kernel learns the model well and performs better than MLR and LASSO. The error evaluation metrics give the small error in the RFR, and this model predicts with the highest accuracy. The performance of DNN is acceptable, but it is not better than RFR. The major features contributing to the efficient performance of RFR are wind speed (27.3%), the span of power lines (20.9%), and wind gust (13.8%), as shown in Table III. These features efficiently and effectively represent the physical power line movement. Therefore, RFR can be substituted as a surrogate model to forecast the clashing score and can be incorporated into practical applications.

2) Comparing the Surrogate Model with Nonlinear Displacement Equations - Surrogate Model Validation: To illustrate the validity of the proposed surrogate model, a comparison between the scores predicted by the surrogate model and the analytical ones obtained from the physical model is presented in Table V, where different power line spans at varying wind speeds, wind gusts, phase clearances, and wind directions are considered. It is noticed that the predicted score is almost equal to the values obtained by the Runge-Kutta (RK) model in all instances. For example, in the second row, the score obtained by the nonlinear displacement model is 0.071429, and the surrogate model predicted score is 0.071428.

The surrogate model predicts the score with 99.99% test accuracy, where 20% of instances are designated to the test dataset with 5-fold cross validation. Therefore, the proposed surrogate model is an accurate representation of the nonlinear conductor displacement method. Comparing the scores obtained by the surrogate model and the mathematical model validates its accuracy in several instances. By utilizing the presented surrogate model based on machine learning, risk scores are obtained instantly, and the high computation burden is no longer an issue. System operators can make informed decisions for PSPS schedule by de-energizing power lines that have ignition scores above a specific threshold.

| $L$ | $d$ | $V_w$ | $V_g$ | Phase clearance (ft) | Angle ($^\circ$) | Score       |
|-----|-----|-------|------|----------------------|---------------|-------------|
| 800 | 33.03| 26    | 26   | 1.5                  | 45            | 0.0714      |
| 500 | 33.03| 18    | 20   | 0.7                  | 45            | 0.0857      |
| 1000| 33.03| 30    | 28   | 0.7                  | 315           | 0.1285      |
| 400 | 33.03| 26    | 14   | 0.9                  | 315           | 0.1714      |
| 300 | 33.03| 30    | 30   | 0.5                  | 315           | 0.4571      |

3) Impact of Various Meteorological and Structural Features on the Conductor Clashing Score: In this part, the surrogate model predicts the clashing score by varying different input features. The conductor clashing scores for different line spans and wind speeds are shown in Fig. 3, where it is illustrated that the clashing scores will be different for various line spans at the same wind speed. Here, the conductor diameter, phase clearance, and angle are kept constant to investigate the effect of power line span and wind speed on the conductor clashing. The increase in wind speed and wind gust leads to an increase in the conductor clashing score. The conductors with a larger span have a lower conductor clashing score for the same wind speed and wind gust because a larger span means conductors are heavier and harder to move. It is noticed that the conductor clashing scores of lines with shorter spans drop with the increase in wind speed above a certain threshold. This is because lighter conductors of various phases will move together at higher wind speeds, reducing conductor clashing. Thus, simultaneous consideration of meteorological and structural features is necessary.

The conductor clashing scores for various phase clearances (P.C) are shown in Fig. 4, where the span, diameter, and angle are set to 1000 ft, 33.03 mm, and 45°, respectively. A smaller phase clearance results in a higher clashing score.
Based on this observation, it is concluded that choosing a one-size-fits-all threshold for wind speed (e.g., 50 mph) for line de-energizing is not a reliable approach.

When wind speed is constant, the conductor clashing score decreases with increasing phase clearances since. With a large phase clearance, the conductors move further apart, and smaller sections of the conductors will slap each other.

### B. WRAP Performance and Comparison Metrics

In this part, the performance of the proposed wildfire-resilient operation framework is investigated. First, WRAP is applied to find the optimal operation schedule of a test 6-bus network. The effectiveness of WRAP in mitigating the wildfire risk of a network under extreme weather conditions is illustrated. We then present two other cases to compare the risk mitigation plans obtained by WRAP with the naive PSPS scenario as well as the method proposed by Rhodes et al. in [26]. The wildfire risk is reduced by de-energizing more power lines, which increases the amount of load shedding. All of the simulations are performed using the Julia [34] programming language, where optimizations are handled with the JuMP [35] module. The average simulation run time for the 6-bus and 30-bus networks is 0.04 second and 0.66 second, respectively.

Implementing WRAP allows system operators to find the optimal schedule for the de-energizing of lines, given the wildfire risk and the penalty parameters. Figure 5 displays the diagram of the test 6-bus grid that is subject to wind. This network has seven lines and two generation units. The wind direction and speed are represented by colored arrows, where the respective wind speed range for each color is shown in the legend. It is observed that this network can be regarded as two regions with severe and mild wind conditions. The wildfire risk score for the lines placed in the mild regions was 0 throughout the whole day. However, the lines in the severe region have a non-zero wildfire risk during most periods of the day. The wildfire risk of these lines changes according to a hypothetical wind curve and only reaches zero during hours 8-17 of the day.
It is noticed that compared with a naive PSPS scenario and the approach proposed by Rhodes et al. [26], WRAP results in considerably lower operation costs. One reason is that WRAP incurs no expected wildfire costs since wildfire risk is maintained at zero in its operations. Additionally, compared with the naive PSPS scenario and the Rhodes approach, WRAP serves the highest amount of demand to consumers. A summary of the results obtained by each of these methods is presented in Table VI. In the naive PSPS approach, utilities shut off power to segments of the network where wildfire ignition risk is deemed high. To simulate the naive PSPS scenario, it was assumed that lines in the extreme wind region are switched off. As a result, the naive PSPS case considers the operation of the network with a fixed configuration where lines 3, 4, and 5 are disconnected, and all of the other lines are kept switched on for the whole duration of the day.

### TABLE VI

| Method                  | Naive PSPS | Rhodes et al. [26] | WRAP |
|-------------------------|------------|--------------------|------|
| Total wildfire risk     | 2.32       | 0                  | 0    |
| Total served demand (MWh) | 2398.56   | 1917.8             | 2760.2 |
| Expected wildfire costs ($x1000$) | 72,696    | 0                  | 0    |
| Percentage of load shedding (%) | 37.47     | 50.0               | 28.04 |
| Total operation costs ($x1000$) | 73,434    | 974.4              | 561.4 |

In addition to a naive PSPS scenario, the performance of WRAP is also compared with the approach introduced in [26]. Rhodes et al. propose a method that integrates the wildfire ignition risk associated with each element of the power system into the optimal operation problem of the network. The model in [26] returns a relative value for the wildfire risk and requires tuning of the control parameter ‘Alpha’. This value adjusts the weight of load serving and wildfire risk in the objective function. The tuning process for this algorithm is displayed in Fig. 7. With the best tuning, this method reduces the wildfire risk to zero. However, it fails to meet 50.0% of the daily demand as opposed to the proposed WRAP method, which only misses 28.04% of the demand. The approach presented in [26] yields a more conservative mitigation plan than the one obtained by WRAP, because it does not account for the implications of weather conditions on wildfire ignition risk.

An analysis of the trade-off between load shedding and fire hazard risk by varying the load-serving percentage ($\alpha$) is presented in Fig. 8. With the gradual change in the value of $\alpha$ from 0 to 100%, load shedding decreases from 1075.4 MWh to 0 MWh, and the cumulative fire hazard risk increases from 0 to 5.15. The increase in the load-serving percentage leads to an increase in objective cost from $0.56M to $230.8M, which signifies the inherent cost of fire hazard risk. It is interesting to observe that by increasing the load-serving percentage from 1% to 50%, the load shedding and cumulative score do not change. This is because the lines that were energized to serve the 1% of demand can still support 50% of demand without needing additional support. Therefore, the fire hazard risk taken into account to serve the load remains unchanged. Another interesting observation in this figure is the jump in risk and load shedding values by raising $\alpha$ from 0 to 1%. When the load serving requirement is set to 0, the system is able to serve 2760.2 MWh of demand without scheduling lines that bear wildfire risk, which results in zero cumulative wildfire risk. However, even if 1% of demand is forced to be served at each location and time interval, the system has to include lines with wildfire ignition risk in its operation.

C. Demonstration of WRAP on the IEEE 30-Bus System

In this section, the presented surrogate model is applied to quantify the risk of wildfire ignition in the modified IEEE 30-bus system during low and high wind speed situations. The network is overlaid on a similar geographical area where the meteorological information can be accessed at [36]. The available meteorological data includes wind speed, wind gust, and wind direction. Other structural features, including the span of line, conductor diameter, and phase clearance, are based on the data of the IEEE 30-bus system. The wildfire ignition score during the low wind speed scenario is shown in Fig. 9. Here, the wildfire ignition score ranges between 0 and 0.06, with the majority of them being 0 due to low wind speed, with the maximum wind speed being 24 mph (11 m/s). The highest risk value of 0.06 belongs to the line connecting buses 6 and 8 because this region has the highest wind speed and gust of 24 mph, causing a relatively higher but still small fire hazard risk.

The wildfire ignition score during a high wind speed scenario is shown in Fig. 10. Here, the maximum wind speed reaches 62 mph (28 m/s), and the fire risk score ranges between 0 and 0.51, where the highest score is associated with the highest wind speed. The aggravating effect of higher
wind speeds on ignition risk is noticeable in these two cases. Although the peak wind speed here is only 2.5 times that in the low wind speed scenario, the maximum cost in the high wind speed scenario is 8.5 times that obtained in the low-speed scenario. The system operator may adjust the value of \( \alpha \) to balance load-serving and the risk value. The presented WRAP model provides a tool for the system operator to balance fire hazard risk and service continuity by leveraging the rendered risk score.

The balance between fire hazard risk and load shedding based on the percentage of enforced load-serving is presented in Fig. 11. In the low wind scenario, at 0% enforced load serving, the objective cost is $193,024 with a load shedding of 8.9% and the cumulative fire hazard risk of 0. As the value of \( \alpha \) is increased, the amount of load shedding is decreased while the wildfire risk is elevated. It is observed that with raising \( \alpha \) from 0% to 10%, load shedding drops to 2.7% while the wildfires risk is increased to 0.7. With 100% enforced load serving, the cumulative fire hazard risk is only 0.81 for the 24 hours of operation.

The system operator’s challenge to balance service continuity with load-serving is more complicated during the high wind speed scenario, as shown in Fig. 11, where the objective cost is $788,187 and load shedding is 41.6% at 0% load serving. The reason behind the difference in the percentage of load shedding in these two scenarios is the difference in the number of lines with a risk score of 0. By increasing the enforced load-serving from 10% to 80%, similar to what was observed in the 6-bus system case, the load shedding and cumulative fire hazard risk remain constant. It is noticed that the fire hazard risk in high wind scenarios sharply escalates when the system is forced to serve any amount of demand, while no further sudden surges are observed as the percentage of the served load is increased, and the load shedding is decreased. This can be associated with the network structure, where to serve an even lower percentage of the load, several lines must become energized. With the 100% enforced load serving, the objective cost is increased to $593.2M, and the fire hazard score is increased to 27.44 for the 24 hours of operation. A summary of the observations in these cases is presented in Table VII.

### D. Wildfire Risk Monetization

The first term in the objective function (6a) aims to monetize the overall wildfire risks. According to [37], the unpredictable nature of wildfire aftermaths makes monetizing the risk of wildfire very challenging. Based on metrics including but not limited to suppression cost, property loss, damage to facilities, rehabilitation costs, the authors in [37] performed a cost analysis on several wildfire instances. The reported statistics suggest that a wildfire could cost between $400-$22,500 per acre. To monetize the risk of wildfires, we incorporated \( K_L \) into our model, a parameter that varies based on the conditions of each region. The monetization values considered for the 33-bus test system are illustrated in Fig. 13. Regions with more facilities and human activity are considered to have higher costs.

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**TABLE VII**

| \( \alpha \) (%) | 0   | 50  | 100 |
|-------------------|-----|-----|-----|
| **Low wind condition** |     |     |     |
| Total wildfire risk | 0   | 0.701 | 0.814 |
| Expected wildfire costs (\( \times 1000\$ \)) | 0   | 6,289.4 | 6,629.9 |
| Percentage of served demand (%) | 91.11 | 97.27 | 100.0 |
| Total operation costs (\( \times 1000\$ \)) | 193.0 | 6,373.3 | 6,664.1 |
| **High wind condition** |     |     |     |
| Total wildfire risk | 0.006 | 27.264 | 27.435 |
| Expected wildfire costs (\( \times 1000\$ \)) | 12.9 | 590,385.8 | 593,162.0 |
| Percentage of served demand (%) | 58.41 | 99.72 | 100.0 |
| Total operation costs (\( \times 1000\$ \)) | 78.8 | 590,429.4 | 593,200.8 |
system operators during pinpoint the power lines that need to be de-energized by service continuity and wildfire risk. With the availability of power lines based on the quantified risk values to balance that enables system operators to schedule the switching of aware operation planning problem, an optimization framework a very high accuracy. We also introduced wildfire risk is developed that quantifies the risk of wildfire ignition associated with the daily operations of each line. It can be observed that larger circles are placed in the lower part of this plot. This observation suggests that implementing WRAP limits the operation schedule of lines with higher ignition risk scores.

Our simulations indicate that WRAP tends to utilize lines that are associated with lower wildfire costs. Results of a case study on the 30-bus system with $\alpha = 50\%$ are presented in Fig. 13. This scatter graph shows the correlation between the wildfire monetization factor of each line and its utilization. It is noticed that lines with higher wildfire costs are not scheduled by WRAP as much as potentially cheaper lines. The size of the filled circles in this figure represents the total amount of risk associated with the daily operations of each line. It can be observed that larger circles are placed in the lower part of this plot. This observation suggests that implementing WRAP limits the operation schedule of lines with higher ignition risk scores.

![Fig. 12. The wildfire risk monetization factor in the IEEE 30-bus system](image1)

Correlation of wildfire monetization factor and daily utilization of line

![Fig. 13. Correlation of wildfire monetization factor and daily utilization of line](image2)

V. CONCLUSIONS

In this paper, a machine-learning-based surrogate model is developed that quantifies the risk of wildfire ignition by power lines under different weather conditions with a very high accuracy. We also introduced wildfire risk aware operation planning problem, an optimization framework that enables system operators to schedule the switching of power lines based on the quantified risk values to balance service continuity and wildfire risk. With the availability of geographical data this tool can be applied to instantly pinpoint the power lines that need to be de-energized by system operators during public safety power shut-off events while allowing flexible decision-making. The results of our method show that compared with the naive public safety power shut-off scenario, the wildfire risk aware operation planning problem schedule reduces wildfire risk and operation costs of the system while increasing the amount of load served. Compared with another approach in the literature, the proposed model reduces operation costs by 42% without increasing the wildfire risk. Several analyses on the control parameter $\alpha$, which determines the amount of critical load, are also performed. A discussion on the wildfire monetization risk factor indicates that wildfire risk aware operation planning problem tends to prioritize utilization of lines with lower costs and limit the operation of high risk lines. Developing a model that is able to incorporate all of the factors that affect the risk of wildfire ignition within a power system such as temperature, humidity, vegetation, topological, and historical data is considered as the extension of this study.

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