Optimization of Composition and Technological Factors for the Lightweight Fiber-Reinforced Concrete Production on a Combined Aggregate with an Increased Coefficient of Structural Quality

Levon R. Mailyan 1, Alexey N. Beskopylny 2,* , Besarion Meskhi 3, Sergey A. Stel’makh 4, Evgenii M. Shcherban 4 and Oxana Ananova 5

1 Department of Roads, Don State Technical University, 344000 Rostov-on-Don, Russia; lrm@aaanet.ru
2 Department of Transport Systems, Faculty of Roads and Transport Systems, Don State Technical University, 344000 Rostov-on-Don, Russia
3 Department of Life Safety and Environmental Protection, Faculty of Life Safety and Environmental Engineering, Don State Technical University, 344000 Rostov-on-Don, Russia; reception@donstu.ru
4 Department of Engineering Geology, Bases, and Foundations, Don State Technical University, 344000 Rostov-on-Don, Russia; sergej.stelm@donstu.ru (S.A.S.); au-geen@mail.ru (E.M.S.)
5 Department of Marketing and Engineering Economics, Faculty of Innovative Business and Management, Don State Technical University, 344000 Rostov-on-Don, Russia; o_ananova@mail.ru
* Correspondence: besk-an@yandex.ru; Tel.: +7-863-273-8454

Abstract: In recent years, developing lightweight concrete with both the necessary and sufficient strength characteristics is essential in the construction industry. This article studies the influence of the volumetric composition of lightweight fiber-reinforced concrete (LFRC) and the method of its distribution during the preparation of the fiber–concrete mixture on the strength and deformation characteristics of LFRC on a combined aggregate. The optimal grain size of the porous filler was calculated by the mathematical planning method of the experiment. Regression models of the strength and deformation characteristics on the volumetric content of fiber and its distribution method were obtained. The most effective combination of these factors has been determined. The model shows that the increase in compressive strength was 12%, the value of the prismatic strength increased by 25%, the bending tensile strength increased by 34%, and the axial tensile strength increased by 12%, and the elasticity modulus increased by 11% compared to the test results of the control composition samples without fiber and pumice. The coefficient of constructive quality (CCQ) of the LFRC on a combined aggregate compared to concrete with the control composition without fiber and pumice showed an increase of more than 32%. It was also found that fiber reinforcement with basalt fibers with a combination of heavy and porous aggregates achieves a synergistic effect together.

Keywords: fiber reinforced concrete; hybrid reinforcement; compressive strength; tensile strength; ultimate deformations; optimal composition

1. Introduction
1.1. The Relevance of Research

The urgency in the problem of the developing lightweight concrete is due to the increasing need for innovative building materials that also have sufficient strength characteristics and significantly lower mass.

High density urban planning and a variety of engineering and geological conditions lead to the need to construct buildings and structures with reduced weight. With an increase in the number of stories and the construction of new large-span and high-rise buildings
with high requirements for the strength and deformability of the building materials, an urgent problem arises regarding the sufficiently durable and at the same time lightweight new generation products [1]. The development of new materials with high strength and low weight is an important scientific problem.

Fiber-reinforced concrete has proven its effectiveness in the construction of basement panels for multi-story buildings [1], fixed formwork to strengthen pile foundations, wall panels and monolithic walls, small architectural forms for the urban beautification architectural decoration of buildings, and many others. However, despite the demand, the scientific problem of the development and application of LFRC remains unresolved and attracts the attention of scientists around the world [1,2].

1.2. Review and Analysis of Literary Sources

One of the technological ways of improving fine-grained lightweight concrete properties is dispersed reinforcement. The work conducted in [3] investigates the strength properties of fine-grained concrete reinforced with amorphous fiber based on the Fe-B-C system and obtained by the “spinning” method. These are concrete types reinforced with available sorts of fiber that are based on mineral wool, basalt fiber, glass fiber, steel, and polypropylene fibers. The best tensile bending strength was shown by samples with amorphous fiber, and the highest compressive strength was shown in samples with steel fiber. The inclusion of amorphous fibers increases flexural strength by 56% but decreases compressive strength by 30% compared to the control samples. The addition of steel fiber shows a 20% increase in flexural strength and a 14% increase in compressive strength, confirming the beneficial effect of adding commercially available fiber to fine concrete. The authors developed compositions of fiber-reinforced concrete with a compressive strength of up to 38 MPa and a bending strength of up to 12 MPa, making it possible to use amorphous fiber as a composition of fine-grained concrete in construction.

The mechanical properties and durability of lightweight concrete based on pumice stone reinforced with basalt fiber and containing nano ground calcium carbonate (GCC) was studied in [4]. Pumice stone is the most promising substitute for heavy aggregate due to its availability, cheapness, and reasonable mechanical characteristics. GCC was used as a replacement for Portland cement in different percentages from 5 to 25% in 5% increments. Basalt fibers 6 mm in length were added in two amounts: 0.5% and 1% by volume. Research results showed that mixes with added GCC had lower mechanical strength at an early age and were comparable to control specimens at a later age. The addition of GCC also decreased water absorption, sorption capacity, and increased resistance to magnesium sulfate compared to a lightweight concrete control. The use of basalt fiber improved the mechanical properties of lightweight concrete based on pumice but worsened the properties of freshly prepared concrete. It was shown that the resulting type of concrete could be used in the industry to produce environmentally friendly concrete blocks along with geopolymer lightweight concrete [5,6].

In [7], the influence of chopped basalt fiber in expanded clay concrete to improve its strength was tested. Experimental dependencies of the concrete behavior under load were obtained using compression and bending tests. Finite element analysis was performed using ANSYS software. The model was developed to test various experimental results that showed that a high percentage of basalt fiber in expanded clay concrete increases its strength. In fact, the direct effect on the nature of destruction was observed on expanded clay concrete without basalt fiber and was then read according to the value of strength and the ultimate deformation of the samples.

Numerical modeling is an effective tool in studying fiber-reinforced concrete with complex properties [8,9]. In article [10], the authors used the ANSYS numerical modeling method to simulate the design parameters of beams, which can be changed depending on the bearing capacity, such as:

- The content of steel fiber in the concrete;
- The distance between steel clamps at the ends of the beam;
• The number of tensile steel rods;
• The diameter of the stretched steel bars,
• Taking into account the nonlinear properties of the materials.

In [11], a study on the inclusion of nanosilica in ultra-lightweight foam concrete (ULFC) was conducted considering the effectiveness of various dosages up to 10 wt.%. The results of the experiments showed that the use of nanosilica in the optimal dosage is an effective way to increase the stability of foam bubbles in the fresh state, to reduce the anisotropy of the pores, and to make it possible to produce foam concrete with an increased wall thickness.

The possibility of using a mixture of cement, fly ash, ground granulated blast-furnace slag, and river sand to produce pre-foamed ultralight composite material (PULC) was investigated in [12]. It was shown that replacing 20% cement with slag resulted in the highest compressive strength as well as the lowest the water absorption value of the PULC samples. The thermal conductivity properties were also numerically investigated, which were inversely proportional to the density of the PULC samples and showed good performance.

Artificial neural networks are actively used to predict the mechanical properties of fiber-reinforced concrete [13–18]. In [19], using artificial neural networks, an analytical model was obtained that describes the final bond strength in terms of the average values of the shear stress. The object of research was concrete of various strength classes that had been reinforced with metal and composite reinforcement. It has been established that the adhesion value is related to the strength characteristics of the concrete and the type of reinforcement used. An artificial neural network technique was proposed in [20] to predict the bond strength of the fiber and cement matrix.

The assessment of the ultimate values of strength and deformability for ultra-high quality fiber reinforced concrete (UHPFRC) elements was conducted in [21–23]. In these studies, an experimental program was implemented on UHPFRC elements by taking into account the influence of the fiber volume fraction, the ratio of shear length to depth, and the compressive strength of the matrix as the main variables. It was shown that the inclusion of steel fiber with a volume fraction of 2% significantly increases the shear and flexural strength of ultra-high foam rubber beams.

1.3. The Objective of the Research

The main aim of the research presented in this article was to develop a dispersed-reinforced lightweight concrete [24–28] that includes both heavy and light aggregate [29]. Thus, a part of the traditional heavy aggregate from dense rocks was replaced by an analogue of lightweight porous filler with equal volume but that was significantly lighter in weight. Granite crushed stone and slag pumice were used as initial components. As a result of the study, a technical problem regarding the reduction of building weight was solved due to the decrease in the density of the concrete while maintaining its strength. Additionally, the problem of reducing building and structure costs was considered since as a result of our recommendations, the proposed concrete significantly decreases the building and structure cost due to the lower cost of slag pumice compared to granite.

Additionally, the aim of this work is to identify and develop proposals for a rational formulation and technology for new materials with an increased coefficient of constructive quality (CCQ). In the scientific and technical literature, CCQ means the ratio of the strength and density characteristics [24–28].

2. Materials

During the experimental research, grade PC 500 D0 Portland cement produced by Oskolcement OJSC was used. Table 1 shows some of the physical and mechanical characteristics of the Portland cement that was used, such as the fineness, the normal consistency, the setting time of the cement paste, and the ultimate bending and compression strength at the ages of 7 and 28 days. Table 2 shows the chemical and mineralogical composition of Portland cement.
Table 1. Physical and mechanical characteristics of Portland cement.

| Portland Cement PC 500 D0 Produced by Oskolcement OJSC | Grinding Fineness, by Specific Surface, cm²/g | Normal Consistency of Cement Paste, % | Setting Time of Cement Paste, min. | Bending Strength, MPa (at the Age of 7 Days) | Compressive Strength, MPa (at the Age of 7 Days) | Bending Strength, MPa (at the Age of 28 Days) | Compressive Strength, MPa (at the Age of 28 Days) |
|----------------------------------------------------------|------------------------------------------------|--------------------------------------|-----------------------------------|---------------------------------------------|---------------------------------------------|-----------------------------------------------|-----------------------------------------------|
| Research methodology                                     | GOST 310.2                                      | GOST 310.3                           | GOST 30744                        | GOST 30744                                  | GOST 30744                                  | GOST 30744                                     | GOST 30744                                     |
| Research result                                          | 2964.2                                         | 28.6                                 | Start—145 finish—240              | 6.0                                         | 26.8                                        | 8.1                                           | 52.4                                         |

Table 2. Mineralogical and chemical composition of Portland cement.

| Cement Grade | Mineralogical Composition, % | Chemical Composition, % |
|--------------|------------------------------|-------------------------|
| PC 500 D0    | C₃S: 68.9, C₂S: 10.9, C₃A: 8.9, C₄AF: 11.3, MgO: 0.9, SO₃: 2.3, Al₂O₃: 4.6, Fe₂O₃: 3.8, Na₂O + K₂O: 0.7, CaO: 60.1, SiO₂: 24.0, Impurity: 3.6 |

Crushed granite was used as a large aggregate, and slag pumice was used as a combined aggregate (Figure 1a,b).

Figure 1. Crushed granite (a) used as a large aggregate and slag pumice (b) used as a combined aggregate.

The physical and mechanical characteristics of crushed stone are presented in Table 3.

Table 3. Physical and mechanical characteristics of crushed stone.

| Fraction | Density, g/cm³ | Bulk Density, kg/m³ | Porosity, % | Content of Dust and Clay Particles, wt. % | Content of Lamellar and Needle-Shaped Grains, wt. % | Crushing, wt. % |
|----------|----------------|---------------------|-------------|------------------------------------------|---------------------------------------------------|---------------|
| 5–20     | 2.85           | 1470                | 45.7        | 0.65                                     | 23                                                | 12.7          |

Quartz sand was used as a fine aggregate, the physical and mechanical characteristics of which are presented in Table 4.

Table 4. Physical properties of fine aggregate.

| Density, g/cm³ | Bulk Density, kg/m³ | Size Module | Porosity, % | Water Demand, % |
|----------------|---------------------|-------------|-------------|-----------------|
| 2.62           | 1480                | 1.4         | 43.3        | 9               |
Table 5 shows the grain densities for the combined mixtures. The mineralogical composition of slag pumice is characterized by:
- Light minerals (80%), which include calcium and magnesium carbonates (68%) and quartz (12%);
- Heavy minerals (18%), represented by onormanite in the form of short square prisms;
- Ferrous sulfate (2%).

| Average Bulk Density of Grains, kg/m³ | Slag Pumice Aggregate Fractions, mm |
|--------------------------------------|-----------------------------------|
|                                       | 5–10 | 2.5–5 | 1.25–2.5 |
|                                       | (1.4–1.5) × 10³ | (1.5–1.8) × 10³ | (1.6–1.8) × 10³ |

Basalt fiber was used as a dispersed reinforcement. Table 6 shows the physical and mechanical characteristics of the used fiber.

Table 6. Physical and mechanical properties of the fiber.

| Basalt Fiber | Tensile Strength, MPa | Fiber Diameter, mm | Fiber Length, mm | Elastic Modulus, GPa | Density, g/cm³ | Elongation Coefficient, % |
|--------------|-----------------------|-------------------|------------------|----------------------|----------------|--------------------------|
|              | 3200                  | 16 × 10⁻³         | 12               | 120                  | 2.6            | 3.2                       |

To regulate the concrete consistency, the superplasticizer Muraplast FK 48 was used (density—1.18–1.21 g/cm³, dosage—0.2–2.0% by weight of cement). It is a highly concentrated, modified condensation product of naphthalene formaldehyde sulfonic acid, does not contain components that cause reinforcement corrosion, effectively disperses the cement paste in the concrete mixture, strongly plasticizes the concrete mixture and reduces its water demand, and reduces the cost of laying and compacting concrete. The recommended consumption of the additive is 1.5% of the cement mass.

3. Methods

The following test equipment was used for this research: a laboratory concrete mixer; a laboratory vibrating platform (type SMZH-539-220A, OOO I-MACH, Armavir, Russia); a hydraulic test press (type IP-1000, Neftekamsk, OOO NPK “TEKHMASH”, Russia) designed for static compression tests of the concrete samples; a universal tensile testing machine (type R-50, OOO I-MACH, Armavir, Russia) for the axial tension testing of the prisms [26,27].

Measurements of the concrete deformations of the test prisms were conducted with a chain of strain gauges with a side length of 50 mm and dial indicators with a graduation of 0.001 mm.

Experimental prisms were tested for axial compression and axial tension at a constant rate of deformation to obtain not only the strength and deformation characteristics of concrete, but also obtain its full deformation diagrams “σ-ε” with a descending curve.

Compression and tensile bending tests were conducted in accordance with the requirements of GOST 10180 “Concretes. Methods for strength determination using reference specimens” [30].

The axial compression and axial tension tests were conducted in accordance with the requirements of GOST 24452 “Concretes. Methods of prismatic, compressive strength, modulus of elasticity and Poisson’s ratio determination” [31].

The experimental research program is shown in Figure 2.
A series is a set of samples made from the same composition. The prism sizes in Figure 1 are in mm.

The process of determining the deformation of a prism sample under axial compression is shown in Figure 3a,b.
Using the method of absolute volumes [32], the initial composition of the concrete mixture was determined:

- Water–cement ratio:
  \[ \frac{W}{C} = \frac{A R_C}{(R_b + 0.5 A R_S)} \]  
  where \( A \) is the coefficient depending on the quality of the materials; \( R_C \) is the activity of the Portland cement; \( R_b \) is the concrete strength.

- The water consumption considering the required mobility determined from the graphs and was \( W = 205 \text{ L/m}^3 \).

- Portland cement consumption, kg/m\(^3\):
  \[ S = \frac{W}{W/C} \]  

- The crushed stone consumption, kg/m\(^3\):
  \[ CS = \frac{1000}{\alpha P_{CS} \rho_{CS} \rho_{CS}} + \frac{1}{R_b} \]  
  where \( \alpha \) is the coefficient of grain spreading; \( P_{CS} \) is the porosity; \( \rho_{CS}^t \) is the true density of the crushed stone; \( \rho_{CS}^b \) is the bulk density of the crushed stone.

- Sand consumption, kg/m\(^3\):
  \[ S = \rho_{CS}^t \left( 1000 - \frac{C}{\rho_C} - \frac{CS}{\rho_{CS}} - W \right) \]  
  where \( \rho_C^t \) is the true density of the sand; \( \rho_C^t \) is the true density of the Portland cement; \( C, CS, \) and \( W \) are the consumption of the Portland cement, crushed stone, and water, respectively.

- The estimated density of the concrete mixture in a compacted state, kg/m\(^3\):
  \[ \rho_{CM} = C + CS + S + W \]  

The parameters of the composition of the concrete mixture obtained as a result of the calculations are reflected in Table 7.

**Table 7. Parameters of the composition of the concrete mixture.**

| Parameter Name | Value | \( W/C \) | \( C, \text{kg/m}^3 \) | \( W, \text{L/m}^3 \) | \( CS, \text{kg/m}^3 \) | \( S, \text{kg/m}^3 \) | \( \rho_{CM}, \text{kg/m}^3 \) |
|----------------|-------|----------|----------------|----------------|----------------|----------------|----------------|----------------|
| Value          | 0.55  | 373      | 205            | 1139           | 720            | 2437           |                 |

The cube compressive strength of the control composition on a dense aggregate was \( R_{b,cub} = 65.2 \text{ MPa} \).

4. Results

The determination of the optimal grain size composition of the porous filler was conducted using the mathematical planning method of the full-factor experiment (FFE 2k) using the program “MathCAD”. The plans were used when the first-order planning did not allow an adequate regression model to be obtained, and the need for its complication became clear. Additionally, it may be used if it is known that the research object has significant nonlinear properties in advance. Compared to plans of the first order, plans of the second order are more complex in structure, have a larger number of points and levels of variation for each factor, and require an increased number of experiments in their implementation.

The parameters were taken as the response function:
- $\rho_b$—bulk density of the slag pumice mixture, kg/m$^3$;
- $\rho_{bv}$—bulk density of vibro-compacted slag pumice, kg/m$^3$ (vibration compaction time 1.5 min);
- $V_{sp}$—the voidness of the slag pumice mixture, %.

The results of experimental studies are presented in Table 8.

Table 8. Results of the slag pumice experimental studies.

| No. | Slag Pumice Fraction Size, mm | Bulk Density of Slag Pumice Mixture, kg/m$^3$ | Bulk Density of Vibro-Compacted Slag Pumice, kg/m$^3$ | Voidness of Slag Pumice Mixture, % |
|-----|-------------------------------|-----------------------------------------------|-----------------------------------------------------|-----------------------------------|
|     | 5–10 ($x_1$) | 2.5–5 ($x_2$) | 1.25–2.5 ($x_3$) | Volume Content of This Fraction, % |                                   |                                   |
| 1   | 1                     | 0                     | 0                     | 968     | 1088 | 37.8 |
| 2   | 0                     | 1                     | 0                     | 1003    | 1130 | 32.3 |
| 3   | 0                     | 0                     | 1                     | 1038    | 1155 | 27.0 |
| 4   | 1/2                   | 1/2                   | 0                     | 1023    | 1110 | 37.0 |
| 5   | 1/2                   | 0                     | 1/2                   | 1115    | 1272 | 14.5 |
| 6   | 0                     | 1/2                   | 1/2                   | 1095    | 1198 | 28.0 |
| 7   | 1/3                   | 1/3                   | 1/3                   | 1096    | 1205 | 26.1 |
| 8   | 3/5                   | 1/5                   | 1/5                   | 1076    | 1196 | 29.4 |
| 9   | 1/5                   | 3/5                   | 1/5                   | 1076    | 1186 | 31.0 |

As a result of statistic processing of the experimental data, a mathematical model was obtained for the bulk density of the mixture of aggregates in its natural state:

$$\rho_b = 968x_1 + 1003x_2 + 1038x_3 + 150x_1x_2 + 448x_1x_3 + 298x_2x_3$$  \(6\)

In the case of a vibrationally compacted mixture of grains, the equation takes the form:

$$\rho_{bv} = 1088x_1 + 1130x_2 + 1155x_3 + 4x_1x_2 + 602x_1x_3 + 222x_2x_3$$  \(7\)

In this case, the porosity of the vibro-compacted mixture was described by the following regression equation:

$$V_{sp} = 37.8x_1 + 32.3x_2 + 27x_3 - 7.8x_1x_2 - 52x_1x_3 - 6.6x_2x_3$$  \(8\)

The resulting equations are graphically presented in Figures 4–6, from which it can be seen that:
- The nature of the change in the bulk density of the mixture in its natural and vibro-compacted state is the same;
- In the vibro-compacted state, the maximum bulk density can reach 1272 kg/m$^3$ and can reach 1115 kg/m$^3$ in the natural state;
- The maximum density and maximum porosity are achieved with discontinuous granulometry (no grains with a fraction of 2.5–5 mm);
- When the relative content of coarse aggregates (5–10 mm) in the mixture is more than 40%, the voidness and bulk density of the mixture is influenced by the fraction of 1.25–2.5 mm;
- With a relative content of a mixture of coarse aggregate (5–10 mm) less than 40%, fluctuations in the number of fine fractions have practically no effect on the voidness and bulk density.
The influence of the porous aggregate on the physical and mechanical properties of compacted concrete in which porous material replaced part of the dense fractions was established by control tests using specimens for axial compression, axial tension, and bending tension. The replacement of the concrete components was conducted at a constant cement consumption rate without changing the total volume of the aggregate mixture.
Figure 6. Dependence of the voidness of a slag pumice mixture on the volumetric content of various types of fractions.

In the studied compositions, up to 50% of the volume of dense aggregate was replaced with the same volume of the porous one.

To identify the most effective grain compositions of the combined aggregates, the combinations shown in Table 9 were investigated. The test results of the concretes made with the indicated grain compositions are presented in Table 9 and Figure 7.

CCQ characterizes the possibility of reducing the weight of buildings while maintaining or even improving the basic properties of materials. The structural quality factor is defined as the ratio of the compressive strength to the relative density $\text{MPa} \times \text{m}^3/\text{kg}$:

$$\text{CCQ} = \frac{R_{b,\text{cub}}}{\rho_{\text{CM}}}$$  \hspace{1cm} (9)

where $R_{b,\text{cub}}$ is compressive strength, MPa;

$\rho_{\text{cm}}$ is the density of the concrete mixture, kg/m$^3$.

SC—designation of the concrete control composition (without slag pumice); S1–S5—designation of the compositions (with different contents of slag pumice).

Table 9. Test results of concrete with different contents of porous aggregate.

| Composition Code | Quartz Sand, % | Granite Crushed Stone, % | Slag Pumice, % | Density, kg/m$^3$ | Compressive Strength, MPa | CCQ, MPa $\times$ m$^3$/kg |
|------------------|----------------|--------------------------|----------------|-------------------|---------------------------|---------------------------|
|                  |                |                          | Fraction, mm   |                   |                           |                           |
|                  |                |                          | 5–10           | 1.25–2.5          |                           |                           |
| cube concrete test specimen (SC) | 100 | 100 | 0 | 0 | 2455 | 65.2 | $26.6 \times 10^{-3}$ |
| S1               | 90             | 90                       | 10             | 10                | 2313                       | 62.9                      | $27.2 \times 10^{-3}$ |
| S2               | 80             | 80                       | 20             | 20                | 2175                       | 60.8                      | $28.0 \times 10^{-3}$ |
| S3               | 70             | 70                       | 30             | 30                | 2035                       | 59.5                      | $29.2 \times 10^{-3}$ |
| S4               | 60             | 60                       | 40             | 40                | 1880                       | 59.1                      | $31.4 \times 10^{-3}$ |
| S5               | 50             | 50                       | 50             | 50                | 1805                       | 52.7                      | $29.2 \times 10^{-3}$ |
Figure 7. Diagram of CCQ for the volume ratio of porous and dense aggregates. SC—the control composition of concrete (without slag pumice); S1–S5—compositions by Table 9.

Analysis of the obtained results and their comparison with the results obtained by other authors [2,8,20,21,33,34] indicates that the inclusion of slag pumice in the composition of concrete instead of as part of the dense aggregates leads to an increase in the CCQ, that is, a decrease in the compressive strength of the concrete is compensated by an even more significant decrease in the density of the material, which means a decrease in mass. The maximum increase of CCQ on the combined aggregate is observed when part of the coarse and small dense aggregate is replaced with slag pumice at 40% of the total volume of these aggregates in the concrete mixture.

Further, this research was conducted to study the strength and deformation characteristics of LFRC on a combined aggregate. Based on preliminary studies, the optimal composition of concrete on a combined aggregate (S4) was determined, which was subsequently used to manufacture LFRC prototypes on a combined aggregate.

The dependence of the change in the strength and deformation characteristics of lightweight fiber concretes on a combined aggregate was studied by changing the volume content of the fiber in the composition of the concrete mixture and the technological methods of its distribution.

As a result of testing the control samples (S4), the strength characteristics of the original concrete were established: $R_{b,cub} = 59.1$ MPa, $R_b = 23.6$ MPa; $R_{bt} = 5.9$ MPa; $R_{btb} = 4.1$ MPa; $\varepsilon_{bR} = 1.87 \times 10^{-3}$ mm/m; $\varepsilon_{btbR} = 1.24 \times 10^{-4}$ mm/m; $E_b = E_{btb} = 35.3$ MPa × 10^3.

The determination of the strength characteristics of LFRC on a combined aggregate was conducted using regression dependencies, the type, and the values of the coefficients that were determined by the mathematical planning methods of the experiment.

As functions, the strength and deformation characteristics of LFRC on a combined aggregate vary depending on the volumetric content of the fiber in the composition of the concrete mixture and its distribution method during the preparation of the concrete fiber-reinforced concrete mixture are taken.

The following parameters were taken as the response function:

- $R_{b,cub} (\mu, t)$—cube compressive strength, MPa;
- $R_b (\mu, t)$—prismatic compressive strength, MPa;
- $R_{bt} (\mu, t)$—bending tensile strength, MPa;
- $R_{btb} (\mu, t)$—axial tensile strength, MPa;
- $\varepsilon_{bR} (\mu, t)$—ultimate deformations during axial compression, mm/m × 10^{-3};
- $\varepsilon_{btbR} (\mu, t)$—ultimate deformations during axial tension, mm/m × 10^{-4};
\[ E_b = E_{btb}(\mu, t) \]—elastic modulus, MPa \( \times 10^3 \).

As variables, the volumetric content of the fiber was taken. The method of its distribution in the preparation of the fiber–concrete mixture in absolute terms with different levels of variation and the values of the various factors are presented in Table 10.

**Table 10.** Values of the variation factors of the FFE 2k.

| N  | Factor Code | The Physical Meaning of the Factor | Unit Measurements | Factor Levels |
|----|-------------|----------------------------------|-----------------|---------------|
| 1  | \( \mu \)   | Volumetric content of fibers \((\mu, \%)\) | %               | –1 0 +1       |
| 2  | \( t \)     | Fiber distribution method         | -               | 1t 2t 3t      |

1t—premixing of cement, water + mixing with fiber + mixing with sand and gravel. 2t—premixing of cement, sand, crushed stone + mixing with fiber + mixing with water. 3t—premixing of cement, sand, gravel, water + mixing with fiber.

The results of experimental studies on the effect of the volumetric content of fiber-reinforced concrete and the method of its distribution in the preparation of a fiber–concrete mixture on the strength and deformation characteristics of LFRC on a combined aggregate are presented in Table 11 and Figures 8–12.

**Table 11.** Results of experimental studies on the influence of the volumetric content of fiber-reinforced concrete and the method of its distribution in the preparation of a fiber–concrete mixture on the physical–mechanical and deformative characteristics of LFRC on a combined aggregate.

| N  | Volumetric Content of Fibers, % | Fiber Distribution Method | \( \rho \), kg/m\(^3\) | \( R_{b,cub} \), MPa | CCQ, MPa/kg \((\times 10^{-3})\) | \( R_b \), MPa | \( R_{bt} \), MPa | \( R_{btb} \), MPa | \( \varepsilon_{bR} \), mm/m \((\times 10^{-3})\) | \( \varepsilon_{btbR} \), mm/m \((\times 10^{-4})\) | \( E_b = E_{btb}, \) MPa \((\times 10^3)\) |
|----|---------------------------------|---------------------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 1  | 1.5                             | 1t                        | 1886            | 56.7            | 30.1            | 25.4            | 6.8             | 3.91            | 1.86            | 1.23            | 35.6            |
| 2  | 2.5                             | 1t                        | 1889            | 58.9            | 31.2            | 26.7            | 7.1             | 4.12            | 1.73            | 1.14            | 38.2            |
| 3  | 1.5                             | 3t                        | 1886            | 57.9            | 30.7            | 24.3            | 6.9             | 4.05            | 1.88            | 1.24            | 35.1            |
| 4  | 2.5                             | 3t                        | 1889            | 59.5            | 31.5            | 27.1            | 7.1             | 4.17            | 1.81            | 1.20            | 36.5            |
| 5  | 1.5                             | 2t                        | 1886            | 62.6            | 32.2            | 27.9            | 7.5             | 4.38            | 1.79            | 1.18            | 36.9            |
| 6  | 2.5                             | 2t                        | 1889            | 64.9            | 34.4            | 28.3            | 7.8             | 4.54            | 1.78            | 1.17            | 37.2            |
| 7  | 2                              | 1t                        | 1888            | 57.5            | 30.5            | 26.1            | 6.9             | 4.03            | 1.85            | 1.22            | 35.8            |
| 8  | 2                              | 3t                        | 1888            | 58.3            | 30.9            | 25.8            | 7.0             | 4.03            | 1.82            | 1.20            | 36.4            |

![Figure 8](image_url)  
**Figure 8.** Change in the compressive strength and the prismatic LFRC on a combined aggregate depending on the volumetric content of fiber-reinforced concrete and the method of its distribution during the preparation of a fiber-reinforced concrete mixture.
Figure 9. Change in the tensile strength in the bending and axial tension of LFRC on a combined aggregate depending on the volumetric content of fiber-reinforced concrete and the method of its distribution in the preparation of a fiber-reinforced concrete mixture.

Figure 10. Change in the ultimate deformations during the axial compression of LFRC on a combined aggregate, depending on the volumetric content of fiber-reinforced concrete and the method of its distribution during the preparation of a fiber-reinforced concrete mixture.
Figure 11. Changes in the ultimate deformations during the axial tension of LFRC on a combined aggregate, depending on the volumetric content of fiber-reinforced concrete and the method of its distribution when preparing a fiber-reinforced concrete mixture.

Figure 12. Change in the modulus of elasticity of LFRC on a combined aggregate depending on the volumetric content of fiber-reinforced concrete and the method of its distribution during the preparation of a fiber-reinforced concrete mixture.

Figures 8–12 show that the largest increase in compressive and tensile strength in bending, prismatic strength, axial tensile strength, elastic modulus as well as the smallest ultimate deformations during the axial compression and tension of fiber-reinforced concrete are observed with the following composition and technological parameters: the volumetric content of basalt fiber is 2%, the method of fiber distribution is 2t (preliminary mixing of
cement, sand, crushed stone + mixing with fiber + mixing with water). This amount of basalt fiber is also confirmed by previous studies [35] and is comparable to the results of similar studies by other authors [2,5,11]. This effective way of distributing the fibers is logical since at first, it is advisable to thoroughly mix the dry components of the concrete mixture and to then evenly distribute the prepared fiber in the resulting mixture and add the water into the ready-made dry fiber–concrete mixture. This method of preparing a fiber-reinforced concrete mixture allows the most uniform distribution of fiber throughout the entire volume of concrete and consequently, ready-made fiber-reinforced concrete with the best strength and deformation characteristics to be obtained, which is in good agreement with similar studies by other authors [2,5,11].

Based on the results of studies using the least squares method, the basic regression equations were obtained, which are presented in the form of polynomials of the 2nd degree:

\[
R_{bcub}(\mu, t) = 60.32 + 0.113\mu + 0.0482 t - 0.15\mu t - 0.7257\mu^2 - 6.5757 t^2
\]

(10)

\[
R_b(\mu, t) = 26.8 + 0.0834\mu - 0.0185 t + 0.375\mu t - 0.554\mu^2 - 2.704 t^2
\]

(11)

\[
R_{bt}(\mu, t) = 7.22 + 0.148\mu + 0.0037 t - 0.025\mu t - 0.0677\mu^2 - 0.7677 t^2
\]

(12)

\[
R_{b:b}(\mu, t) = 4.2 + 0.0091\mu + 0.0044 t - 0.0225\mu t - 0.029\mu^2 - 0.434 t^2
\]

(13)

\[
\varepsilon_{bR}(\mu, t) = 1.72 - 0.0067\mu - 0.0037 t + 0.0025\mu t + 0.1064\mu^2 + 0.0964 t^2
\]

(14)

\[
\varepsilon_{b:bR}(\mu, t) = 0.97 - 0.0026\mu - 0.002 t + 0.1064\mu^2 + 0.1249 t^2
\]

(15)

\[
E_{bR} = E_{b:bR}(\mu, t) = 36.78 - 0.0796\mu - 0.0296 t - 0.3\mu t - 0.5888\mu^2 - 1.5388 t^2
\]

(16)

Figures 13 and 14 show diagrams of compression “\(\varepsilon_{b}-\sigma_{b}\)” and tension “\(\varepsilon_{b:b}-\sigma_{b:b}\)” for the control composition concrete (S4) and for LFRC on a combined aggregate with the best strength and deformation characteristics.

![Figure 13. Diagram of the state of compressed concrete (S4—control composition; LFCCA—LFRC on a combined aggregate).](image-url)
5. Discussion

A comparison of the results was conducted with the data from the study of the mechanical and strength properties of the lightweight pumice concrete reinforced with basalt fiber (BPLC) containing nano-ground calcium carbonate (GCC) [2]. GCC was used as a standard substitute for Portland cement in the amounts of 5%, 10%, 15%, 20%, and 25%, and 6-mm long basalt fibers were added in two grades of 0.5% and 1% by volume. Experimental results showed that at an early age, the mixture with GCC had lower mechanical strength results; however, it was comparable in strength to the reference mixes at a later age. The addition of GCC also decreased water absorption, sorption capacity, and showed an increase in magnesium sulfate resistance compared to the reference lightweight concrete. The use of basalt fiber improved the mechanical properties of BPLC, but the inclusion of the fiber reduced the properties of the fresh concrete.

However, in [2], porous substitutes for coarse aggregate made of dense rocks, which create a frame and provide the bearing capacity of concrete, have not been studied.

The research work that [5] presents is an experimental study of the mechanical behavior of structural expanded clay concrete from basalt fiber. The main purpose of this study [5] was to check the effect of crushed basalt fiber in expanded clay concrete to increase its strength, that is, its absolute characteristics. However, [5] did not study the relative physical and mechanical characteristics, in particular, it did not determine the coefficient of constructive quality, that is, the most important characteristic for and lightweight concrete.

The aspects noted above are widely disclosed and highlighted by us in this study.

As a result of the analysis of Figures 13 and 14, the following was established: Based on the obtained deformation diagrams, the peak with displacement up and to the left of the diagram is presented in the deformation of LFRC on a combined aggregate. On the other hand, the remaining diagrams of the control concrete compositions had a lower peak with a shift to the right. Thus, based on the analysis of the data obtained on the deformation of the tested sample, it can be concluded that the recommended composition and technological methods for controlling the strength and deformative characteristics of LFRC on a combined aggregate are advisable.

According to the results of experimental studies on the influence of the volumetric content of fiberglass and the method of its distribution in the preparation of a fiber-reinforced
Concrete mixture on the strength and deformation characteristics of LFRC on a combined aggregate, the most effective combination of these factors was determined. As such, with the inclusion of basalt fiber at 2% of the volume of the concrete mixture where the fiber distribution was conducted according to the 2t method (preliminary mixing of cement, sand, crushed stone + mixing with fiber + mixing with water), the best values of the strength and deformation characteristics of LFRC are observed in the combined filler. Thus, in comparison to the values obtained when testing the control samples, the increase in compressive strength was 12%, the value of the prismatic strength increased by 25%, the tensile bending strength increased by 34%, and the axial tensile strength increased by 11%. The ultimate deformations during axial compression decreased by 10%, decreased by 12% during axial compression tests, and the modulus of elasticity increased by 11%. Cement consumption remained unchanged.

CCQ of LFRC on a combined aggregate is $35.3 \times 10^{-3} \text{ MPa} \times \text{m}^3/\text{kg}$. This concrete is the most effective in terms of construction since in comparison to traditional heavy concrete, it has a sufficiently high strength at a lower density value. The coefficient of constructive quality of concrete on dense aggregate is $26.6 \times 10^{-3} \text{ MPa} \times \text{m}^3/\text{kg}$, and for the control composition concrete S4, it was $31.4 \times 10^{-3} \text{ MPa} \times \text{m}^3/\text{kg}$. Thus, selecting a rational grain size composition for the porous aggregate and its ratio with the dense aggregate made it possible to achieve a CCQ increase of more than 18% compared to the control composition on the dense aggregate. In turn, the recipe-technological methods for controlling the characteristics of LFRC on a combined aggregate proposed in this study led to an increase in the CCQ by more than 32% compared to the control composition on dense aggregate and by more than 13% compared to the control composition S4.

Thus, in comparison with the values obtained when testing the control samples, the increase in compressive strength was 12%, the value of the prismatic strength increased by 25%, the tensile bending strength increased by 34%, and the axial tensile strength increased by 11%. The ultimate deformations during axial compression decreased by 10% and by 12% with axial tension, and the elasticity modulus increased by 11%. Cement consumption remained unchanged.

6. Conclusions

As a result of our research, we made the following conclusions: It has been established that using the technology of combining aggregates, namely replacing part of a dense, heavy, expensive granite aggregate that is of a similar volume but lower in density (by 20–30%) and, consequently in cost, aggregate, for example, such as slag pumice, it is possible to achieve preservation and in some cases with certain rational combinations of technological and recipe parameters, an increase in structural and deformative characteristics, an improvement in the quality of concrete as a whole, and at the same time, a significant reduction in the weight of the structure due to a decrease in the mass and density of the concrete. This increases the coefficient of constructive quality of such concretes.

At the same time, in the study, rational combinations of technological and recipe parameters were determined, various combinations were investigated and were expressed as a percentage, representing the ratio between a dense aggregate and its porous analogue, which are combined in the concrete while having a positive effect on the general properties of the reinforced concrete structures made in such a way.

It was also found that fiber reinforcement with basalt fibers gives a synergistic effect together with the combination of aggregates that are both heavy and porous.

Thus, using a complex recipe solution that includes a combination of a combined aggregate and basalt fiber, we significantly reduce the weight of the structure, achieve resource and material savings, energy savings in the production and manufacturing of such products and structures as well as increase the strength characteristics, reduce the deformability, and achieve a positive effect in the construction of buildings and structures in general.
Quantitative analysis can be assessed by the increase in such indicators as the coefficient of structural quality for the investigated type of concrete in comparison to control samples made from control compositions. Thus, the increase was up to 32%.

Methodologically, the results obtained here can be substantiated as follows: Due to the use of lighter initial components—less dense aggregates—we achieved a smaller concrete mass, which is expressed as a sharp decrease in one of the main parameters. At the same time, by improving the recipe-technological processes and factors, we achieved an increase in strength, that is, an absolute increase in relation to the control composition. Thus, we justify the increase in the coefficient of constructive quality from the point of view of the methodology and that is expressed in the technological and recipe aspects and, ultimately, in the operational aspect.

Thus, it can be concluded that there is a significant effect resulting from a complex combination of aggregates and basalt fibers in concrete, thus obtaining a promising concrete: lightweight concrete on a combined aggregate with basalt fiber reinforcement.

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