Enhanced Adsorptive Desulfurization Using Mongolian Anthracite-Based Activated Carbon
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ABSTRACT: This study reports usage of Mongolian anthracite-based porous activated carbons (PMACs), namely, PMAC 1/3 and PMAC 1/4 for model diesel fuel desulfurization, having 500 ppmw of dibenzothiophene (DBT) in n-heptane. Further, the effects of contact time, adsorbent dosage, and temperature on the adsorption capacity were studied systematically. The experimental adsorption isotherm results were well represented by the Sips isotherm for PMAC 1/3 and the dual site Langmuir isotherm for PMAC 1/4. The maximum DBT adsorption by PMAC 1/3 and PMAC 1/4 were 99.7 and 95.7%, respectively. The kinetics for the adsorption of DBT on PMACs follows the pseudo second order behavior. The Weber–Morris plot shows the multilinearity over the entire time range, suggesting that both the surface and pore diffusions control the adsorption. The values of boundary layer thickness for PMAC 1/4 and PMAC 1/3 were found to be 3.183 and 1.643, respectively. Thus, PMAC 1/4 possesses more surface diffusion control than PMAC 1/3. The changes in Gibbs free energy (ΔGº), entropy (ΔSº), and enthalpy (ΔHº) are negative, which confirms that the studied process is spontaneous and exothermic and possesses less randomness at the interface. Based on the Sips isotherm, single-stage batch-adsorber design was prepared for the adsorption of DBT onto PMAC 1/3.

1. INTRODUCTION
The refractory sulfur compounds present in crude oil are becoming costlier for refiners worldwide. The increase of sulfur content in the crude oil and the strict norms on sulfur emission from diesel vehicles have made the desulfurization issue more serious.¹–⁴ The diesel sulfur content should be less than 10 ppm by 2020 as per the latest regulations in India. The major challenges for refiners in India are to meet the fuel sulfur specifications as well as reduce the aromatic content.⁵,⁶

Hydrodesulfurization (HDS) is a well-established process for desulfurization of liquid fuels.⁷ However, it involves severe operating conditions and sensitive as well as most advanced catalysts to produce diesel with sulfur content less than 10 ppm, making the process expensive.⁷,⁸ There are limitations for the HDS process to remove benzothiophene, dibenzothiophene (DBT), and alkyl substituent DBT.⁹ Therefore, the other available desulfurization options involving oxidation, extraction, biochemical, and adsorption methods have been considered to produce ultralow-sulfur diesel to meet the new environmental regulations.⁷–¹⁶ Among these methods, adsorptive desulfurization (ADS) has gained more attention because the adsorption technique is simple to operate and can be done even under ambient conditions. Various research groups have studied liquid-based ADS using different adsorbents.¹⁶–²² The main challenge for the ADS process is to synthesize high adsorptive capacity adsorbents. In addition, adsorbents employed must possess thioselectivity for the heavy refractory sulfur compound adsorption that needs severe conditions to

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remove using the HDS process. In the past, several activated carbons (ACs) produced from coal and biomass were used.\textsuperscript{16,23–25}

ACs are the most celebrated adsorbents for their application in separation and purification technologies because of their worthwhile surface properties.\textsuperscript{26,27} ACs have also become very popular for ADS because of their microstructure.\textsuperscript{28,29} The adsorption performance of ACs depends upon the adsorbent surface properties. In general, pore volume, specific surface area, pore size, and pore size distribution of an adsorbent play an important role in ADS.\textsuperscript{26,30,31} However, the surface properties do not always have linear relation with the desulfurization capabilities\textsuperscript{32} and therefore, to further enhance the adsorptive capabilities of adsorbents, researchers have impregnated ACs with metal halides.\textsuperscript{26,29,32} In addition, it has been stated that the ADS performance of AC greatly depends on the precursor materials used and preparation methods.\textsuperscript{33}

The carbon-rich, high bulk density Mongolian raw anthracite (MRA) with less ash content can be possibly used for producing adsorbents for ADS, as ACs from MRA have been already successfully tested for methane adsorption and capacitor applications.\textsuperscript{34,35}

In the present study, novel Mongolian anthracite-based porous ACs (PMACs) were tested for sulfur removal from of the model diesel fuel (MDF) (DBT dissolved in \textit{n}-heptane). It may be noted here that ADS using PMACs has not been reported yet according to the best of our knowledge. The adsorption results of DBT on PMAC 1/3 as well as PMAC 1/4 are presented in this report. The Sips, Langmuir, and dual site Langmuir isotherm models were used to study the equilibrium adsorption behavior of DBT on PMACs. The adsorption kinetics of DBT on PMACs was studied using the pseudo first order, pseudo second order, and diverse diffusion models. Further, the thermodynamics of the adsorption system was investigated to determine the values of $\Delta H^\circ$, $\Delta G^\circ$, and $\Delta S^\circ$. At last, a batch adsorption process design has also been proposed based on the results obtained.

2. Experimental

2.1. Materials. The method of preparation for the adsorbents PMAC 1/3 and PMAC 1/4 used in this study is given elsewhere.\textsuperscript{35} The surface properties of the prepared PMACs are as follows: specific surface area (PMAC 1/3: 2038 m$^2$/g and PMAC 1/4: 2784 m$^2$/g), average pore volume (PMAC 1/3: 1.31 cm$^3$/g and PMAC 1/4: 2.27 cm$^3$/g), and average pore diameter (PMAC 1/3: 2.00 nm and PMAC 1/4: 2.20 nm).\textsuperscript{35} The adsorbents were dried in a hot air oven at 110 °C for 12 h before every adsorption study. Beside these ACs, the chemicals used in this study, namely, DBT of purity >98% and \textit{n}-heptane of purity >99% were purchased from Sigma-Aldrich Pvt ltd., India.

2.2. Model Diesel Fuel. For the preparation of the MDF, 0.1982 g of DBT was added into 100 mL of \textit{n}-heptane as purchased without any further purification. The concentration of DBT is selected such that the total sulfur concentration should be 500 ppm by weight.

For investigating the selectivity of DBT over aromatic compounds, equimolar concentration of two polyaromatic hydrocarbons, namely, naphthalene and fluorene and one monoaromatic hydrocarbon, namely, ethylbenzene with different weight percentages (2, 4, 6, 8, and 10 wt %) were added into the MDF. The aromatic added MDFs were named MDF-A-$\alpha$ where $\alpha$ varies from 2 to 10 wt %. Because \textit{n}-heptane has volatile nature; therefore, to avoid a change in the sulfur concentration, the prepared MDF was stored in amber vials.

2.3. Adsorption Equilibrium. The adsorption of DBT on PMACs was done at 30 °C and 250 rpm. In a typical experiment, 20 mL of MDF was taken in an Erlenmeyer flask with a known amount of the adsorbent (0.025–0.40 g). The mixture of MDF and the adsorbent was agitated in an Incubator shaker for 1 h. The DBT concentration in the desulfurized samples was analyzed by a gas chromatograph equipped with a flame ionization detector (PerkinElmer Clairs S80, GC-FID) after separating the adsorbent using a whatman paper. GC is equipped with a Elite-1 (length 50 m and inner diameter 200 μm) flame ionization detector as well.

The quantity adsorbed $q_e$ (mg-S/g-A) was given by the eq 1 as below

$$ q_e = (C_0 - C_e) \times \frac{V}{W} $$

where $q_e$ is the quantity of sulfur adsorbed (mg-S/g-A), $C_0$ is the initial concentration of sulfur (mg-S/L-MDF), $C_e$ is the equilibrium concentration of sulfur after the removal of sulfur by adsorption (mg-S/L-MDF), $V$ and $W$ are the volume of MDF (L) and $W$ is mass (g) of the adsorbent, respectively.

The percentage of sulfur removed was calculated using the following equation

$$ \% \text{sulfur removal} = \left( \frac{C_0 - C_e}{C_0} \right) \times 100 $$

2.4. Data Analysis. To check the fitness accuracy of models, data analysis was done using the coefficient of determination ($R^2$), nonlinear error functions, residual root mean square error (RMSE), and chi-square test ($\chi^2$). The empirical equations used for this study are as follows

$$ R^2 = 1 - \frac{\sum_{n=1}^{n} (q_{e,n} - q_{m,n})^2}{\sum_{n=1}^{n} (q_{m,n})^2} $$

$$ \text{RMSE} = \sqrt{\frac{1}{n-1} \sum_{n=1}^{n} (q_{e,n} - q_{m,n})^2} $$

$$ \chi^2 = \sum_{n=1}^{n} \frac{(q_{e,n} - q_{m,n})^2}{q_{e,n}} $$

where $q_e$ and $q_m$ is the experimental and predicted value of the amount of sulfur adsorbed, respectively, and $n$ is the number of observations. The data analysis was done based on the linear and nonlinear coefficient values. The $R^2$ value closer to unity and lower values of RMSE and $\chi^2$ generally show that the predicted and experimental values fitted well. The average relative error (ARE) and normalized standard deviation (NSD) were employed to check the fitness of kinetic models. Generally, lower values of NSD and ARE indicate better model fitting. The equations for the calculation of NSD and ARE are given as follows

$$ \text{NSD} = 100 \times \sqrt{\frac{1}{N-1} \sum_{i=1}^{N} \left( \frac{q_{e,i} - q_{m,i}}{q_{e,i}} \right)^2} $$
\[
\text{ARE} = \frac{100}{N} \sum_{i=1}^{N} \left[ \frac{q_{t,e} - q_{t,m}}{q_{t,e}} \right]
\]

where \(q_{t,e}\) is the experimental and \(q_{t,m}\) is the theoretically calculated quantity of sulfur adsorbed on PMACs.

3. RESULTS AND DISCUSSION

3.1. Effect of the Adsorbent Dosage. The removal capacity of sulfur was studied for different doses of adsorbents using MDF containing 500 ppm of total sulfur content. The dosage was taken in the range of 0.025—0.4 g of adsorbent for 20 mL of MDF as shown in Figure 1. Sulfur removal was rigorously increased with increasing adsorbent weight from 0.025 to 0.25 g. Thereafter the removal efficiency has become constant for the adsorbent dose greater than 0.25 g for PMAC 1/3 and PMAC 1/4. The relative successive S-removal is small compared to removal with the initial adsorbent dosage. This shows that the equilibrium has been reached between the adsorbate and adsorbent under the operating conditions. It shows the solid concentration effect or particles overcrowding.

3.2. Equilibrium Isothermal Adsorption. The adsorption isothermal analysis was conducted using the MDF with a fixed initial sulfur concentration of 500 ppm and the adsorbent dosage varies from 2.5 to 40 g/l for 1 h at 30 °C. Figure 2 shows the relationship of the equilibrium amount of DBT adsorbed on the surface of PMAC 1/3 and PMAC 1/4 against equilibrium DBT concentration. As shown in Figure 2, \(q_e\) increases with \(C_e\) and reaches saturation which is the maximum adsorption capacity for PMAC 1/3 (\(\sim 2.489 \text{ kmol/kg}\)) and PMAC 1/4 (\(\sim 2.183 \text{ kmol/kg}\)).

The observation of heterogeneity and homogeneity of the solid surface, calculation of adsorption energy, interaction between the fluid compound and solid phase adsorbent and the type of coverage were observed by the plot between \(C_e\) (kmol/m\(^3\)) versus \(q_e\) (kmol/kg). The increased adsorption is because of more surface area and adsorption sites with an increasing adsorbent quantity from 0.025 to 0.4 g. The maximum DBT adsorption by PMAC 1/3 and PMAC 1/4 were 99.7 and 95.7%, respectively, as shown in Figure 1, for 0.4 g of the adsorbent in 60 min. The sample PMAC 1/3 showed relatively higher adsorptive capacity though PMAC 1/3 having a smaller surface area as compared to PMAC 1/4. The probable reason of higher removal using PMAC 1/3 could be its higher micropore volume fraction (66.4%) available as compared to PMAC 1/4 (42.2%). The DBT molecule size (0.8 nm) is more closer to the pore diameter of PMAC 1/3 (2.0 nm) than PMAC 1/4 (2.2 nm) which allows PMAC 1/3 to preferentially adsorb more DBT molecules. Table 1 shows the ADS capabilities of various adsorbents. It can be observed that the adsorptive capacity of PMACs synthesized in this work have potential to adsorb the DBT molecule significantly.

3.3. Aspen Adsorption Isotherm Modelling. The DBT and n-heptane properties were evaluated by the Peng–Robinson equation of state (PR-EOS) thermodynamic model. The PR-EOS is given as under

\[
P = \frac{RT}{v - b} - \frac{a}{v(v + b) + b(v - b)}
\]

where \(a\) and \(b\) are binary interaction parameters and depend on the critical properties as mentioned below

\[
a = \frac{0.45724(RT_c)^{2/3}}{P_c} \left[ 1 + m(1 - T_i^{0.5}) \right]^2
\]

\[
b = 0.0778 \frac{RT_c}{P_c}
\]

3.3.1. Langmuir. In its formulation, Langmuir presumes monolayer adsorption that can only takes place at a finite number of definite localized, identical, and equivalent sites. These sites have no steric hindrance. The Langmuir isotherm is given by the following equation

\[
q_e = \frac{q_m c_m}{K + c_m}
\]
energy of adsorbate and 2, respectively, and patche. In addition, each site has di assumptions for the Langmuir model are applicable at each respectively. The heterogeneous adsorbent is formed by two used to describe the adsorption behavior on the heterogeneous
structure. The goodness of fit of isotherm models with the experimental data was checked using the calculated values of $\chi^2$ and RMSE, which are given in Table 2. The data obtained from error analysis confirmed the best fit of Sips for PMAC 1/3 and dual site Langmuir for PMAC 1, respectively.

### Table 1. DBT Adsorption Capacities of Different Adsorbents at Room Temperature

| Adsorbent | Surface Area (m²/g) | Adsorption Time (min) | Adsorption Capacity (mg/g) | Initial Sulfur Content (ppm) | Ref |
|-----------|---------------------|-----------------------|-----------------------------|------------------------------|-----|
| Microwave-synthesized carbon nanotubes | 171.0 | 60 | 21.50 | 250 | 61 |
| AC-2200 | 493.0 | 90 | 8.60 | 150 | 15 |
| AC-WS | 1570.0 | 30 | 47.10 | 220 | 62 |
| ACFH-Cu+2 | 1090.0 | 480 | 19.00 | 330 | 63 |
| Mesoporous carbon-silica nanocomposite via copper modification | 276.0 | 2880 | 13.95 | 960 | 64 |

where $q_e$ is the heterogeneity factor. If the value of $n_i$ is greater than 1 then it is heterogeneous. The Sips characteristics parameter is $b$ and is in (kJ/mol)$^{1/n_i}$.

All the isotherms were employed to analyze the adsorption equilibrium behavior of DBT on PMACs using Aspen Adsorption 8.4. The equilibrium adsorption data of DBT on PMAC 1/3 and PMAC 1/4 at 30 °C are shown in Figure 2. The goodness of fit of isotherm models with the experimental data was checked using the calculated values of $\chi^2$ and RMSE, which are given in Table 2. The data obtained from error analysis confirmed the best fit of Sips for PMAC 1/3 and dual site Langmuir for PMAC 1, respectively.

### Table 2. Adsorption Isotherm Parameters

| Isotherms | PMAC 1/3 | PMAC 1/4 |
|-----------|----------|----------|
| Langmuir | $q_m = 2.701$ | $q_m = 2.936$ |
| $K_r = 1890.620$ | $K_r = 306.981$ | |
| $R^2 = 0.976$ | $R^2 = 0.960$ | |
| $\chi^2 = 2.124$ | $\chi^2 = 0.502$ | |
| RMSE = 0.027 | RMSE = 0.003 | |
| Dual Site Langmuir | $q_m = 6.83$ | $q_m = 3.109$ |
| $b_1 = 2.520 \times 10^{-4}$ | $b_1 = 2.730 \times 10^{-3}$ | |
| $b_2 = 2.215$ | $b_2 = 4.410 \times 10^{-1}$ | |
| $b_3 = 1.470 \times 10^{-1}$ | $b_3 = 8.950 \times 10^{-2}$ | |
| $R^2 = 0.968$ | $R^2 = 0.990$ | |
| $\chi^2 = 1.360$ | $\chi^2 = 0.014$ | |
| RMSE = 0.024 | RMSE = 0.001 | |
| Sips | $q_m = 4.629$ | $q_m = 6.300$ |
| $b = 8.138$ | $b = 7.602$ | |
| $n_1 = 0.390$ | $n_1 = 0.570$ | |
| $R^2 = 0.986$ | $R^2 = 0.975$ | |
| $\chi^2 = 0.101$ | $\chi^2 = 0.028$ | |
| RMSE = 0.007 | RMSE = 0.002 | |

### 3.4. Effect of Contact Time.**

The adsorbent size, the coefficient of diffusion, and the degree of mixing decides the quantity and rate at which the adsorbate adsors on the surface of the adsorbent. MDF with DBT concentration 500 ppm were kept in contact with PMAC 1/3 and PMAC 1/4 for 2 g/l adsorbent amount at room temperature for 10–90 min. After 60 min a steady state was achieved and a quasi-equilibrium situation was obtained for both the adsorbents as shown in Figure 3. The adsorption rate rapidly increased in the earlier
stage of experiments because of free sites available for adsorbates to adsorb on the surface. The initial fast adsorption depicts that the number of active sites available are more, and it slows down at equilibrium because of the few available sites and the mutual repulsive forces between the adsorbate present in the solution and at the surface of the adsorbent.48

3.5. Adsorption Kinetic Studies. The kinetic study is vital for designing an adsorption system. In the initial stage of adsorption meso- and macro-pores gets saturated with DBT molecules. Thereafter, the adsorption rate gets slowed down when the DBT molecules traverse further deep into the microspores and experience larger resistance in the later stage.49 Thus, to get a better understanding of DBT adsorption on PMACs, pseudo first order and the second order models were used to obtain the kinetics data.

3.5.1. Pseudo First Order Kinetics. Pseudo first order kinetics assumes that DBT molecules are nondissociating on the surface of PMACs and no DBT molecule is present initially on the surface of the adsorbents PMAC 1/3 and PMAC 1/4. The pseudo first order kinetics is given by50,51

\[ q_t = q_e (1 - e^{-kt}) \]  

where \( q_e \) and \( q_t \) are sulfur adsorbed at equilibrium and at time \( t \). \( k_1 (1/\text{min}) \) is the rate constant of pseudo first order adsorption.

3.5.2. Pseudo Second Order Kinetics. It is given by52

\[ q_t = \frac{(k_2q_e^2 \cdot t)}{1 + (k_2q_e^2 \cdot t)} \]  

The linear \( \log(q_e - q_t) \) versus \( t \) was used for the pseudo first order kinetic model and the \( t/q_t \) versus \( t \) plot was used for the pseudo second order kinetic model as shown in Figure 4. The estimated kinetic parameters are given in Table 3. Lower values of ARE and NSD and higher values of \( R^2 \) values generally show the good fitting with the experimental data. It was observed that DBT removal by PMACs follows pseudo second order kinetics.

3.6. Diffusion Mechanism. The adsorbate transportation from bulk solution to the adsorbent surface may be controlled by single or multiple mechanisms,53 that is, film or external diffusion, surface diffusion, pore diffusion, or a combination of two. The system controlled by film diffusion may have poor mixing, lower adsorbate concentration, small adsorbent particle size, and higher affinity between the adsorbate and adsorbent. Similarly, the intraparticle diffusion controls the system where the mixing is proper, high adsorbate concentration and lower affinity of the adsorbate for the adsorbent.54

\[ B_i = -0.4977 - \ln(1 - F) \]  

\[ F = 1 - \frac{6}{a^2} \exp(-B_i) \]  

where \( F = q_t/q_e \) is the fraction of equilibrium attained, \( B_i \) is the function of \( F \).

The diffusion mechanisms affecting the kinetics are given by Weber’s intraparticle and Boyd’s surface diffusion model.55 The intraparticle diffusion-controlled mechanism is given by

\[ q_t = k_{ip}t^{1/2} + C \]  

where \( k_{ip} \) is the coefficient of intraparticle diffusion (mg/g(min)^{1/2}) and \( C \) depicts the boundary layer thickness (boundary resistance). The surface diffusion controller mechanism is defined by Boyd’s kinetic expression.56

The intercept and slope of the linear plot \( q_t \) versus \( t^{0.5} \) given in Figure 5a are calculated to obtain the intraparticle diffusion coefficient \( K_{ip} \) and boundary resistance \( C \), respectively. If the overall adsorption data exhibit multilinear plots, then two or more steps control the diffusion. As shown in Figure 5a, PMAC 1/3 and PMAC 1/4 plots are not linear for the overall range; this concludes that one or more processes are influencing the adsorption. Hence, the adsorption process follows a complex mechanism, having both surface and intraparticle diffusion within the pores of PMAC 1/3 and PMAC 1/4.57

The initial and final linear portion shows the surface adsorption58 and intraparticle diffusion effect57 respectively. The nearly parallel segment of the plots suggests the comparability of adsorption rates for DBT into the PMAC pores at all temperatures. Further, to find the slowest step between intraparticle and surface diffusion, the Boyd kinetic model, eq 20, was used to further examine the kinetic data. The \( R^2 \) values of Boyd’s plots given in Figure 5b, for both PMAC 1/3 and PMAC 1/4 confirms that the plot is linear. Thus, surface diffusion seems to be the rate-controlling step in the adsorption for both PMAC 1/3 and PMAC 1/4. The intercept values are given in Table 4. As given in the table the boundary layer thickness of PMAC 1/4 is greater than that of PMAC 1/3; thus, PMAC 1/4 is more surface diffusion controlled compared to PMAC 1/3. This conclusion is also well supported by the scanning electron microscopy (SEM) images of PMAC 1/3 and PMAC 1/4, as shown in Figure 6,
PMAC 1/3 is more porous in nature and therefore, it has lower surface diffusion resistance for the DBT molecule to be adsorbed on the surface than PMAC 1/4. This result also explains the less pore diffusion-controlling mechanism for PMAC 1/3.

3.7. Thermodynamic Studies. The temperature effect on DBT adsorption on PMACs was studied as presented in Figure 7. It was found that with increasing temperature sulfur removal decreases as shown Figure 7a. The reduction in adsorption of DBT on PMACs with increase in temperature shows that the adsorption is following physisorption phenomena. The ΔG° was calculated by using eq 21 whereas ΔS° and ΔH° were determined from the intercept and slope of the linear Van’t Hoff plot between ln Kd and 1/T as shown in Figure 7b, which depicts the thermodynamic behavior of the adsorption process.

The ΔG° was evaluated by the given equation

ΔG° = −RT ln Kd

(21)

Kd = DBT concentration adsorbed
    DBT concentration remained in the solution

where ΔG° is the change in Gibb’s free energy, Kd is the distribution coefficient, R is the gas constant and T is
temperature in K. The Van’t Hoff equation was used to calculate the $\Delta H^o$ and change in entropy $\Delta S^o$

$$\ln K_d = \left(\frac{\Delta S^0}{R} - \frac{\Delta H^0}{RT}\right)$$ (22)

Thermodynamic parameters of the system are shown in Table 5. The negative $\Delta G^o$ value confirms spontaneity and feasibility of the system.45 The negative values of $\Delta H^o$ confirm that the overall adsorption process is exothermic in nature. Negative $\Delta S^o$ values indicate the decrease in the degree of freedom of the adsorbed DBT molecule on PMACs.48

3.8. Design of Batch Sorption from Isotherm Data.
The single-stage batch adsorption system can be designed using the adsorption isotherm. A schematic diagram is shown in Figure 8 considering the volume of MDF, $V$ (L); the DBT concentration reduces from $C_0$ to $C_1$ (mg/L), the DBT loading changes from $q_0$ to $q_1$ (mg/g), and the amount of adsorbent is $M$ (mg). At time $t = 0$, $q_0 = 0$ and as time passes the mass balance equates DBT removed from the MDF to that picked up by the solid. The mass balance equation for the system shown in Figure 8a is

$$V(C_0 - C_1) = M(q_0 - q_1) = Mq$$

(23)

Under equilibrium conditions $C_1 \rightarrow C_e$, $q_1 \rightarrow q_e$.
Because the Sips isotherm fits the equilibrium data for DBT onto PMAC 1/3, the Sips isotherm equation can be used to modify the batch adsorber design equation as presented below

$$\frac{M}{V} = \frac{(C_0 - C_e)}{q_i} = \frac{(C_0 - C_e)}{q_e} = \frac{C_0 - C_e}{q_{i, Sips}} \frac{q_{Sips}}{1 + \frac{q_{Sips}}{C_e}}$$

(24)

Figure 8b shows the plot between the predicted amount of PMAC 1/3 needed to remove different percentages of DBT from the MDF of initial concentrations 500 mg/L at different solution volumes. The design procedure is defined for a single-stage batch sorption system. For example, the quantity of PMAC 1/3 required for the 90% removal of DBT from the MDF of concentration 500 mg/L was 97.21, 194.43, 291.64, and 388.84 mg for MDF volumes of 1, 2, 3, and 4 L, respectively.

3.9. Effect of Aromatics on DBT Removal. It is a well-known fact that the aromatic compounds present in diesel generally compete with the sulfur-bearing compounds to occupy the adsorption sites of most of the adsorbents. Therefore, further study was conducted to investigate the effect of aromatics present in MDF-A-$\alpha$ on DBT adsorption. The effect of aromatics present in the MDF-A-$\alpha$ is shown in Figure 9. It can be observed from the figure that the adsorption of aromatic compounds increases with increasing the dosage of the adsorbent. The highest adsorption after DBT is shown by aromatic compounds which may inhibit the sulfur removal capacity of the adsorbent. To understand the inhibiting effect of aromatics, different weight % of the aromatics was used and their effect on sulfur removal was examined as shown in Figure 10. It was noted that the increasing aromatic concentration negatively impacted the sulfur uptake of the adsorbents. This arises because of competitive adsorption between DBT and the aromatics resulting in decrease in sulfur uptake. Similar to the results of sulfur removal from the MDF using PMACs 1/3 and 1/4, PMAC 1/3 shows better performance for the removal of sulfur from MDF-A-$\alpha$.

4. CONCLUSIONS
In this work, DBT adsorption capacity of PMACs has been studied. The study shows that the desulfurization ability of PMAC 1/3 (84.56 mg/g) exhibits better performance compared to PMAC 1/4 (74.25 mg/g). The higher desulfurization capabilities of PMAC 1/3 have direct correspondence with the better microporosity. PMAC 1/3 follows Sips and PMAC 1/4 follows the dual site Langmuir

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**Table 5. Thermodynamic Parameters for the Adsorption of DBT on PMAC 1/3 and PMAC 1/4**

| $T$ (°C) | $K_d$ PMAC 1/3 | $K_d$ PMAC 1/4 | $\Delta G^o$ (Kcal/mol) PMAC 1/3 | $\Delta G^o$ (Kcal/mol) PMAC 1/4 | $\Delta H^o$ (Kcal/mol) PMAC 1/3 | $\Delta H^o$ (Kcal/mol) PMAC 1/4 | $\Delta S^o$ [Kcal/(mol. K)] PMAC 1/3 | $\Delta S^o$ [Kcal/(mol. K)] PMAC 1/4 |
|---|---|---|---|---|---|---|---|---|
| 40 | 5.099 | 3.572 | $-4.244$ | $-3.317$ | $-14.890$ | $-0.037$ | $-24.760$ | $-0.065$ |
| 50 | 3.372 | 2.948 | $-3.267$ | $-2.907$ | $-14.890$ | $-0.037$ | $-24.760$ | $-0.065$ |
| 60 | 2.825 | 2.354 | $-2.877$ | $-2.372$ | $-14.890$ | $-0.037$ | $-24.760$ | $-0.065$ |
| 70 | 2.153 | 2.214 | $-2.189$ | $-2.269$ | $-14.890$ | $-0.037$ | $-24.760$ | $-0.065$ |

**Figure 8.** (a) Single-stage batch-adsorber design for PMAC 1/3 (b) adsorbent mass (M) against volume of solution treated (L) at 303.15 K.
adsorption isotherms model. The diffusion of DBT in PMACs follows a complex diffusion model which means both intraparticle and surface diffusions. In addition, DBT adsorption on PMACs follows pseudo second order kinetics. The thermodynamic studies revealed that the adsorption of DBT on PMACs is an exothermic and spontaneous process having less randomness at the interface. Further, the present study significantly indicates that the aromatics affects the adsorption of DBT on the PMACs.

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