X-ray spectral studies of TeV $\gamma$-ray emitting blazars

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ABSTRACT

This work is a summary of the X-ray spectral studies of 29 TeV $\gamma$-ray emitting blazars observed with Swift/XRT especially focusing on sources for which X-ray regime allows to study the low and the high energy ends of the particle distributions function. Variability studies require simultaneous coverage, ideally sampling different flux states of each source. This is achieved using X-ray observations by disentangling the high-energy end of the synchrotron emission and the low-energy end of the Compton emission, which are produced by the same electron population. We focused on a sample of 29 TeV $\gamma$-ray emitting blazars with the best signal-to-noise X-ray observations collected with Swift/XRT in the energy range of 0.3-10 keV during 10 years of Swift/XRT operations.

We investigate the X-ray spectral shapes and the effects of different corrections for neutral hydrogen absorption and decompose the synchrotron and inverse Compton components. In the case of 5 sources (3C 66A, S5 0716+714, W Comae, 4C +21.35 and BL Lacertae) a superposition of both components is observed in the X-ray band, permitting simultaneous, time resolved studies of both ends of the electron distribution. The analysis of multi-epoch observations revealed that the break energy of X-ray spectrum varies only by a small factor with flux changes. Flux variability is more pronounced in the synchrotron domain (high-energy end of the electron distribution) than in the Compton domain (low energy end of the electron distribution). The spectral shape of the Compton domain is stable, while the flux of the synchrotron domain is variable. These changes cannot be described by simple variations of the cut-off energy, suggesting that the high-energy end of the electron distribution is not generally well-described by cooling only.

Key words: Radiation mechanisms: non-thermal --- Galaxies: active --- BL Lacertae objects: general --- Galaxies: jets

1 INTRODUCTION

BL Lacertae (BL Lac) type objects as well as Flat Spectrum Radio Quasars (FSRQ) constitute a class of Active Galactic Nuclei (AGN). In a unified model, these are the sources characterized by polarized and highly variable non-thermal continuum emission observed from the jet pointing at small angles to the line of sight (e.g., Begelman et al. 1984). The radiation observed extends from radio wavelengths up to the X-ray regime, or even - in the case of the most energetic sources - up to high and very high energy $\gamma$-ray range (e.g. Wagner 2009, Vercellone et al. 2011, H.E.S.S. Collaboration 2013c, 2014). The emission observed from blazars is known to be variable at all wavelengths on different timescales down to hours or even minutes in the most extreme cases (e.g. Wagner & Witzel 1995, Aharonian et al. 2007c, Gopal-Krishna et al. 2011, Saito et al. 2013, Liao & Bai 2015). Also, flux changes in blazars are often associated with spectral variability (e.g. Xue et al. 2006, Böttcher et al. 2010, Gaur 2014).

The spectral energy distribution (SED), in $\nu\nu F_\nu$ representation, shows in most cases two broad emission components. The low energy peak is usually attributed to synchrotron radiation of relativistic electrons from the jet, while the origin of the high-energy peak still remains matter of debate. In the most common leptonic scenarios, the high-energy bump is explained as inverse Compton radiation from the same population of relativistic electrons scattering either the synchrotron photons (SSC, Synchrotron Self Compton models; e.g. Maraschi et al. 1992, Kirk et al. 1998) or external photons from the surroundings, e.g. accretion disc, broad lines region or dust (EC, External Compton
models: e.g. Dermer et al. (1992) Sikora et al. (1994). Alternatively, the high-energy peak can be explained in the framework of hadronic scenarios. In this case the high-energy radiation is produced in processes such a proton synchrotron emission, synchrotron and Compton emission from secondary decay products of charged pions, or \( \pi^\pm \) decay (Aharonian 2000 Atoyan & Dermer 2003 Mücke et al. 2003 Böttcher et al. 2013). Additionally, Petropoulou & Mastichiadis (2015) have shown that Bethe-Heitler emission can explain SED of blazars in the case when the typical double-humped structure is not clearly visible.

Depending on the frequency of the low-energy peak, BL Lac type blazars can be subdivided into high-, intermediate- and low-energy peaked objects: HBL, IBL, LBL, respectively (see, e.g. Padovani & Giommi 1995 Fossati et al. 1998 Abdo et al. 2010). For LBL type blazars the synchrotron peak is located in the infrared regime (\( \nu_s \leq 10^{14} \) Hz), for IBL blazars in the optical-UV range (\( 10^{14} \) Hz < \( \nu_s \leq 10^{15} \) Hz), while for HBL blazars in the X-ray domain (\( \nu_s > 10^{15} \) Hz) (Abdo et al. 2010). It has been proposed and connected with decreasing bolometric luminosities and \( \gamma \)-ray dominance by Fossati et al. (1998). According to the blazar sequence, HBL blazars are synchrotron dominated, while FSRQs are \( \gamma \)-ray dominated. In the later work the concept of the blazars sequence has been updated with a large sample of radio-loud AGNs to the blazars envelope (Meyer et al. 2011).

The different classes of blazars could also be distinguished according to the location of the X-ray spectrum in SED. For HBL type blazars the X-ray spectrum is usually located in the synchrotron domain. While in the case of IBL type sources the X-ray emission usually covers both synchrotron and inverse Compton component. For several IBL type sources the upturn of SED located in the X-ray domain has been reported e.g. BL Lacertae (Tanahata et al. 2000 Ravasio et al. 2002 Donato et al. 2005), W Comae (Tagliaferri et al. 2000 Donato et al. 2005), SS 0716+71 (Cappi et al. 1994 Giommi et al. 1999 Tagliaferri et al. 2003 Donato et al. 2005 Ferrero et al. 2006 Wierzchowska & Siejkowski 2015 AO 0235+16 (Raiteri et al. 2006), OQ 5710 (Tagliaferri et al. 2003), 3C 66A (Donato et al. 2005). LBL type objects are usually characterised with the X-ray spectrum covering the inverse Compton bump. The X-ray observations of the brightest HBL type blazars unfolded strong variability often with large amplitudes of variations, observed on long as well as on short timescales (Sembay et al. 1993 Tanahata et al. 2000 Sembay et al. 2002 Zhang et al. et al. 2002 2005). In several mentioned cases HBLs variability amplitudes have been also found to be correlated with the energy. Furthermore, HBL blazars are known for “harder-when-brighter” behaviour manifested in hardening of spectral index with the increasing flux level observed (e.g. Pian et al. 1998 Zhang et al. 2005 2006 H.E.S.S. Collaboration 2012).

The X-ray variability studied in different energy bands seem to be correlated, often with time-lags of a few hours. Usually variations observed in lower energies have lags behind those at higher energies (so-called soft time-lags), but the opposite (so-called hard time-lags) are also observed (e.g. Zhang et al. 2006 Fossati et al. 2000). Furthermore, the comparison of X-ray spectral index (\( \alpha \)) and flux intensity (I) presented in a \( \alpha-I \) plots reveals clockwise (for soft time-lags) or counter-clockwise (for hard time-lags) patterns (e.g. Takahashi et al. 1996 Ravasio et al. 2004 Brinkmann et al. 2005). The time-lags are directly related with changes of acceleration and cooling time scales (Kirk et al. 1998).

The X-ray variability observed in the case of IBL and LBL type objects show similar behaviour according to the variability time scales and amplitudes observed for HBL type blazars. But, for these classes of blazars, as opposed to HBL type ones, the variability amplitudes seem to be anticorrelated with the emission energy (e.g. Giommi et al. 1999 Ravasio et al. 2002). Furthermore, in mentioned studies no time-lags between the low and the high energy X-ray emission has been observed.

Previous studies focusing on the nature of the X-ray spectra disclosed its complex nature and several authors discussed features of blazars behaviour in this domain. Worral & Wilkes (1990) analysed large sample of BL Lac type blazars observed with Einstein which were well described with the single power-law model with a wide range of spectral indices. This model as well as the broken power-law one were also successfully used to describe the X-ray spectra in the later works for data collected with different instruments like ASCA (e.g. Kubo et al. 1998), BeppoSAX (e.g. Wolter et al. 1998 Padovani et al. 2001 2004), HEAO-1 (e.g. Sambruna et al. 1994) and ROSAT observations (e.g. Perlman et al. 1996 Urry et al. 1996 Sambruna et al. 1996).

Alternatively, in a several works the X-ray spectra are well described with the curved log-parabola model. Inoue & Takahara (1996), Tavecchio et al. (1998), Giommi et al. (2002) Donato et al. (2005) studied the X-ray observations of blazars performed with BeppoSAX and found this model as preferable for at least 50% of the sources analysed. In the later studies Massaro et al. (2004a,b) 2006 analysed the X-ray spectra for Mrk 421 and Mrk 501 and found the log-parabola as the best model for characterization of their spectra in different activity states. The authors also suggested a possible interpretation of the mentioned model in term of statistical particle acceleration with the assumption that the probability of the increase of particles energy is a decreasing function of an energy. Furthermore Massaro et al. (2008) enlarged their sample to 15 objects and found the log-parabola as the best model for most of the blazars spectra studied.

The mentioned studies revealed that the X-ray spectra are characterized with a wide range of spectral indices. Following the distributions presented by Donato et al. (2005), which are consistent with the previous and the later studies by e.g. Perlman et al. (2005) Tramacere et al. (2007) Massaro et al. (2008), the X-ray spectral indices of HBL type blazars are between \( \Gamma_X = 1.8 \) and \( \Gamma_X = 3.0 \), for LBL type objects this quantity is between \( \Gamma_X = 1.5 \) and \( \Gamma_X = 1.8 \), while in the case of FSRQs, spectra are best described with the spectral indices between \( \Gamma_X = 1.0 \) and \( \Gamma_X = 2.0 \).

The motivation of this work is to test if the X-ray spectra observed with Swift/XRT in the energy range of 0.3-10 keV are well described with the single power-law model or the continuously curved log-parabola. Both characteristics are reasonable and widely discussed in the context of models used for description of synchrotron ageing and acceleration processes (e.g. Leahy 1991 Massaro et al. 2004a,b). Also, we would like to check for how many of selected TeV emitting blazar the X-ray regime is a place, where the low- and the high-energy spectral component meet or if the X-
ray spectral shape allows us to predict where this point for particular blazars is located in broadband SED. Finally, different values of the Galactic column absorption provided in several surveys (Dickey & Lockman 1990; Kalberla et al. 2005; Willingale et al. 2013) give us reason to study, which values are preferable and how changes in the Galactic column density values influence the X-ray spectral properties.

The paper is organized as follows: the Swift Gamma-Ray Burst Mission is described in Sect. 2, while Sect. 3 gives information about the sample selection and data analysis. All selected sources are described in Sect. 4, Sect. 5 focusses on 5 blazars, for which an upturn point is visible in the X-ray regime. The work is summarized in Sect. 6.

2 THE SWIFT GAMMA-RAY BURST MISSION

The Swift Gamma-Ray Burst Mission (hereafter Swift) (Gehrels et al. 2004), launched in November 2004, is a multi-wavelength space observatory, equipped with three instruments: the Burst Alert Telescope (BAT, Barthelmy et al. 2005), the X-ray telescope (XRT, Burrows et al. 2005) and the Ultraviolet/Optical Telescope (UVOT, Roming et al. 2005). Swift/XRT operates in the energy range of 0.3-10 keV.

The XRT detector can be operated in different modes: the Windowed Timing (WT), the Photon Counting (PC) and the Imaging (IM); the forth - Photo-Diode mode - is not working since May 2005. In the PC mode the full CCD chip is read out every 2.5 seconds and it is used for sources with count rate smaller than 1 count per second. Observations provided in this mode have full imaging and spectroscopic resolution. The WT mode is characterized by 1.7 ms time resolution and full energy resolution. The mode is usually used to observe the sources with count rate larger than 1 count per second. During the monitoring of a chosen source, the detector can switch between the PC and the WT mode, to optimize the observations. The third, Imaging mode is used only to obtain the first X-ray position of a newly detected Gamma Ray Burst.

3 SAMPLE SELECTION AND DATA ANALYSIS

The catalogue of TeV sources (TeVCat) includes 167 objects and 58 of them are classified as blazars. All of the blazars were observed several times with Swift/XRT. The main properties of the TeV blazars, as well as the total exposure in the PC mode and integrated flux for the energy range of 0.3-10 keV obtained using the online analysis of Swift/XRT data (Evans et al. 2009) are collected in Table 1.

Since the aim of this work is to focus on properties of the average X-ray spectra for particular blazars, the further analysis has been limited to objects with the best Swift/XRT data for which the product of the integrated flux and the exposure is greater than 3.0 ⋅ 10^{-10} erg cm^{-2}.

This allowed to single out 29 objects with high signal-to-noise level, and for which Swift/XRT data allow to obtain good-quality spectra. The sources chosen are marked in the last column in Table 1. One object, namely, IC 310, fulfilled our criteria but it is not included in our sample, since in the literature it is not classified as a blazar, but as a radio-galaxy or a transition object between radio galaxy and BL Lac type source (e.g. Kadler et al. 2012; Aleksic et al. 2014d).

This study is limited to observations taken in the PC mode, since data taken in the WT mode are affected by charge redistribution problems inherently related to the way in which the CCD of the instrument is read. These depend on the position of the source on the CCD before binning the read out on a 10 pixel basis and makes the response position-dependent. The effect is small for mildly absorbed sources, but in this study we focus on long time integrated spectra, so a number of photons is huge and it can be seen as an impact on the residuals in spectra. The effect was also noticed in Swift/XRT observation in WT mode by e.g. Massaro et al. (2008).

For 29 selected blazars Swift/XRT data were analysed using HEASoft package v. 6.16 software with CALDB v. 20140120. All events are cleaned and calibrated using the xrtpipeline task. Data in the energy range of 0.3-10 keV with grades 0-12 are analysed. For the spectral studies, data are grouped using the grappa tool to have a minimum 20 counts per bin and the co-added spectra are fitted using XSPEC v. 12.8.2 (Arnaud 1996).

In the first step two models were used to fit Swift/XRT spectrum:

- a single power-law defined as
  \[
  \frac{dN}{dE} = N_p \left( \frac{E}{E_0} \right)^{-\Gamma},
  \]
  with the Galactic absorption,
- a logarithmic parabola defined as
  \[
  \frac{dN}{dE} = N_l \left( \frac{E}{E_0} \right)^{-(\alpha + \beta \log(E/E_0))},
  \]
  with the Galactic absorption.

Here, the power-law model is characterized by the normalization \(N_p\) and the spectral index \(\Gamma\) (at energy \(E_0\)), while the log-parabola model is described with the normalization \(N_l\) and the curvature parameter \(\beta\) and the spectral index \(\alpha\) (at energy \(E_0\)). In both cases the scale energy \(E_0\) is fixed at 1 keV. In each case four different values of the Galactic absorption parameter are tested:

- \(N_{HI}^{LAB}\) taken from the Leiden Argentine Bonn Survey (LAB, Kalberla et al. 2005). The survey gives an information about \(N_{HI}^{LAB}\) values for different region of the sky. The map was obtained by merging two surveys: the Leiden/Dwingeloo Survey (Hartmann & Burton 1997) and Instituto Argentino de Radioastronoma Survey (Arnal et al. 2000; Bajaja et al. 2005). The beamsize is 36 arcmin for declinations \(> -27.5\) deg and 30 arcmin for declinations \(< -27.5\) deg. The uncertainties are in each case at a 2-3% level.

1 http://tevcat.uchicago.edu/
2 The number of objects collected in catalogue up to June 2015.
3 Private communication by Sergio Campana.
4 http://heasarc.gsfc.nasa.gov/docs/software/lheasoft
Different models and $N_H$ values tested lead to the conclusion that in the most cases of TeV $\gamma$-ray emitting blazars the preferable description of the X-ray spectrum is the log-parabola model. Only in the cases 1ES1101-232, Mrk 180 and PKS 2005-489, the F-test values imply that the average spectrum is best fitted with a single power-law model.

The preferable fits do not allow us to distinguish a best, universal $N_H$ value, which could be used in all cases. In the sample of 29 sources we found that the values taken from LAB, [Willingale et al. 2013], Dickey & Lockman [1990] are preferable in 6, 8, 5 sources, respectively, while in the other 10 cases, a free $N_H$ value provides the best $\chi^2_{red}$ result. The selection of the preferable model and $N_H$ value was based not only on the fit to the X-ray data characterised with $\chi^2_{red}$, but also in divergent cases we investigate the shape of the fitted spectrum in the context of the overall broadband spectral energy distribution built from archival data. In the sample studied there are a few objects (such like PKS 0548-322, H 1426+428 or PKS 2155-304) for which different $N_H$ value result in a very similar X-ray spectral curvature. But there are also several cases for which different surveys provide different Galactic column density values, which result in very different spectral curvatures. An extreme example is 1ES0033+595 (see in Fig. 5). In several cases spectra with very different characterisations are fitted with very similar values of $\chi^2_{red}$.

In our collection of 29 X-ray spectra we found that the shape of spectra is characterised with $\alpha$ or $\Gamma$ (depending on the preferred model of the spectrum) in the range 1.3-2.6. For the fit with a log-parabola model the curvature parameter $\beta$ lies between $-0.100$ and $-0.347$ for the concave curved spectra and between 0.066 and 0.477 for the convex curved spectra. Below, main properties of the X-ray spectra for the selected 29 objects in the context of our and previous studies are discussed:

4.1 Notes on individual objects

1ES 0033+595: The X-ray spectrum of this blazar is well described with the log-parabola model ($\chi^2_{red} \sim 1.0$). The power-law fits result in $\chi^2_{red} \sim 1.8$ and it is less favoured. Comparing different values of the Galactic column density, we conclude that the best fit to data is obtained using fixed $N_H$ value provided by [Willingale et al. 2013] or with free $N_H$ value. A low value of $N_H$, e.g. from Kalberla et al. [2005] or [Dickey & Lockman 1990], causes an artificial bump in the synchrotron component in SED. 1ES 0033+595 is an extreme example of a source for which different $N_H$ values used result in significant changes in the spectral shapes, while $\chi^2_{red}$ values differ only slightly.

Previous studies of the X-ray observations of 1ES 0033+595 with BeppoSAX by [Giommi et al. 2002] also favour the log-parabola model for the description of the X-ray spectrum, with $\alpha = 1.4$ and $\beta = 0.4$. These results are consistent with the ones obtained in this paper in the case of log-parabola fit with $N_H$ value taken from [Willingale et al. 2013]. [Donato et al. 2005] claimed a power-law as a good model for later BeppoSAX observations with spectral data.
index of $\Gamma = 2.1$ and free $N_H$ value significantly smaller than $N_H$ values from discussed surveys.

**RGB J0136+391:** The X-ray spectrum of the blazar is well characterized with the log-parabola model with all $N_H$ values tested or with the power-law with free $N_H$ value and the one provided by Willingale et al. (2013). The preferable fits result in $\chi^2_{red}$ of about 0.9, while in the latter case $\chi^2_{red}$ is about 1.3. Donato et al. (2001) found single power-law with free $N_H$ value as the favourable model for this source.

**3C 66A:** The X-ray spectrum for the blazar is best described with the log-parabola model ($\chi^2_{red} \sim 0.95$). For the comparison the power-law model fitted to data result in $\chi^2_{red} \sim 1.1-1.2$. Negative values of the $\beta$ parameter in all log-parabola fits confirm the concave curvature of the fitted model and indicate that the turning point of SED is located in the Swift/XRT energy range. We found the break energy value of $(3.4 \pm 0.3)$ keV by fitting also the broken power-law model to data. We also found $N_H$ value from Kalberla et al. (2005) as the best one for the blazar. The log-parabola fit with free $N_H$ results in parameter value significantly smaller than the ones provided by the surveys considered.

In the previous studies Donato et al. (2005) found power-law with free $N_H$ value or curved power-law as preferable description of X-ray spectrum. We note that in the latter case the curvature is not significant. The spectral indices mentioned by the authors ($\Gamma = 2.2-2.4$) is about 5% smaller than results presented in this paper.

**1ES 0229+200:** In the case of this blazar the comparison of the log-parabola and the power-law fits slightly favours description of the spectrum in the X-ray domain with the first ones. The log-parabola model result in $\chi^2_{red} \sim 1.16$, while the power-law one results in $\chi^2_{red} \sim 1.20-1.38$. Regarding the different values of the Galactic column density tested, the value taken from Kalberla et al. (2005) survey is preferred.

In the previous studies the curvature of the spectrum in the X-ray domain was also suggested by Massaro et al. (2008) for observations obtained with BeppoSAX, XMM-Newton and Swift/XRT. The results obtained by authors are consistent with results from this paper with $N_H$ value from Willingale et al. (2013) survey. Donato et al. (2005) analysed the BeppoSAX observations of the blazar and found the power-law model with free $N_H$ value as the best one for this source. The spectral index obtained by Donato et al. (2005) is $\Gamma = 2.0$, and it is significantly larger than values from this paper.

**PKS 0447−439:** The spectrum in the X-ray range for this source is well described with the log-parabola model with $\chi^2_{red} \sim 1.1$. For the comparison the power-law model fitted to data results in $\chi^2_{red} \sim 1.2-1.4$. With different values of $N_H$ tested the one provided by Dickey & Lockman (1990) is found as the best one.

In the previous studies of the X-ray data collected with Swift/XRT H.E.S.S. Collaboration (2013b) described the blazar spectrum with the power-law model with the spectral index $\Gamma = 2.8-3.3$. The authors did not find any significant improvement when using the broken power-law model.

**1ES 0502+675:** The X-ray spectrum for this blazar can be equally well characterized using either the power-law fit or the log-parabola one. For the case of the power-law model satisfying fit parameters are obtained using free $N_H$ value or the one provided by Willingale et al. (2013), and in both cases $\chi^2_{red} \sim 1.0-1.1$. For the log-parabola fit also the same $N_H$ gives the best $\chi^2_{red} \sim 1.0$ values. For the case of the log-parabola model fitted with $N_H$ values provided by Kalberla et al. (2005) and Dickey & Lockman (1990) we got also acceptable fits with $\chi^2_{red} \sim 1.1$. Different amounts of $N_H$ are compensated by different degrees of curvature $\beta$.

No need for curved model for the description of the BeppoSAX observations was found by Donato et al. (2005). The authors favour the single power-law description of the X-ray spectrum, with the spectral index of 2.3. This value is similar to the one from our study for the case free $N_H$ value.

**PKS 0548−322:** The spectrum is well described with both a log-parabola and a power-law model. For the log-parabola model we do not find any preferable value of $N_H$. In each case the spectral fits result in very similar values of the spectral parameters and a $\chi^2_{red}$ of about 1.0. In the case of the power-law fit with a free $N_H$ value or the one taken for Willingale et al. (2013). Fits give a $\chi^2_{red}$ of about 1.0-1.1.

Donato et al. (2005) found that both a power-law and a log-parabola can characterize the X-ray spectrum with the spectral indices of about 2.3-2.4. Giommi et al. (2002) prefer the log-parabola model for BeppoSAX observations with spectral index of 1.5 and the curvature parameter 0.5. For the comparison in this paper the preferable spectral index is 1.7 and the curvature parameter about 0.2.

The studies of several BeppoSAX, XMM-Newton and Swift/XRT observations of the source performed by Massaro et al. (2008) confirmed that the X-ray spectrum has a curved log-parabolic shape. Also, Aharonian et al. (2010) found the broken power-law model with spectral indices of 1.7 and 2.0 and the break energy of 1.7 keV as better than the power-law one for the case of Swift/XRT observations of the blazar.

**1ES 0647+250:** The source is well described with the log-parabola model. Different values of $N_H$ results in similar $\chi^2_{red}$ value of about 1.1, while in the case of the power-law model $\chi^2_{red}$ is in the range of 1.2-2.0, depending on $N_H$ value used. 1ES 0647+250 is an example of a blazar, for which in the case of the log-parabola fit very similar $\chi^2_{red}$ values for different $N_H$ tested reveal significantly different curvatures with $\beta$ in the range from 0.17 up to 0.45.

**S5 0716+714:** The Swift/XRT spectrum is well described by a log-parabola model with $\chi^2_{red}$ of about 1.0. For the comparison the single power-law model tested gives $\chi^2_{red}$ of about 1.2. Different values of $N_H$ in the case of the log-parabola fit show slightly similar concave curvature with $\beta$ of about $(0.22)-(0.15)$. Also the broken power-law one gives a reasonable fit with $\chi^2_{red}$ of 1.2. In this case the break energy is found as $E_b = (1.10 \pm 0.10)$ keV.

The curvature of the spectrum in the X-ray domain has been suggested in several studies. Tagliaferri et al. (2003), Ferrero et al. (2006) and Donato et al. (2005) found a broken power-law model as the preferable one with energy break of 1.5 keV, 1.5-5.3 keV and 1.75-2.73 keV respectively.
1ES 0806+524: The best characterisation of the shape of the X-ray spectrum for this blazar is given using either the log-parabola fit, with any of tested $N_H$ values, or with the power-law model, with a free $N_H$ value. For all the log-parabola fits and the single power-law with free $N_H$, $\chi^2_{red}$ is around 1.0. Previous studies focusing on the Swift/XRT observations of 1ES 0806+524 did not reveal a need for a curved model. Acciari et al. (2009). The authors describe source with the power-law model with spectral index of 2.5-2.7, which is consistent with the results from this paper.

1ES 1011+496: The spectrum of 1ES 1011+496 can be well characterized using the log-parabola model with any of considered $N_H$ values. The models fitted result in $\chi^2_{red}$ of about 0.9-1.0. For the single power-law model $\chi^2_{red}$ is in the range of 1.3 and 1.6, depending on $N_H$ value chosen. The previous studies of the Swift/XRT observations by Reintjes et al. (2012) show data that are well fitted with the power-law model.

1ES 1101−232: The X-ray spectrum is well described using the power-law as well as the log-parabola models, in both cases with any of $N_H$ values tested. In all cases $\chi^2_{red}$ for each of the $N_H$ value tested is about 1.0. In the case of this blazar values of $N_H$ taken from different surveys result in very similar fit parameters ($\alpha$, $\beta$, $\Gamma$).

Donato et al. (2005) found a log-parabola as the preferred model for the X-ray spectrum obtained using BeppoSAX observations. Also Massaro et al. (2008) favour the curved model, characterized with $\alpha = 1.6-1.9$ and $\beta = 0.3$.

Mrk 180: All spectral fits with a log-parabola model with any of $N_H$ values tested here result in reasonable $\chi^2_{red}$ value. A good fit to data is obtained with a power-law model, but only with free $N_H$ value($\chi^2_{red}\sim 1.0$). The previous observation of the source obtained with BeppoSAX are well described with the log-parabola model with $\alpha = 2.1$ and $\beta = 0.4$.

Giommi et al. (2002).

RX J1136.5+6737: The power-law model is a good description of the X-ray spectrum of this blazar ($\chi^2_{red} \sim 1.0$). This spectrum is also well characterized with the log-parabola model. In the first case $\chi^2_{red}$ is about 1.0, while in the latter 1.1. No preferable $N_H$ value has been found for this source either in the case of single power-law model fitted or the log-parabola one.

1ES 1218+304: The log-parabola model result in similar values of $\chi^2_{red} \sim 1.2$ for the different values of $N_H$ tested. Also, in the case of the power-law different values of $N_H$ tested give comparable results $\chi^2_{red} \sim 1.3$. In both cases, the curvature and the spectral parameters of the fits do not differ significantly.

The log-parabola model is the favourable one for the spectrum characterization for BeppoSAX Donato et al. (2005), XMM-Newton Massaro et al. (2008) and Swift/XRT observations Tramacere et al. (2007), Massaro et al. (2008). Furthermore Giommi et al. (2002) found that BeppoSAX observations in the X-ray range can be well described with a sum of two power-law models.

W Comae: The log-parabola model is a more plausible scenario for the X-ray spectrum characterization ($\chi^2_{red}$ of about 1.0). Since W Comae is fitted with concave curvature, in order to find the break energy for this source, we also fitted the X-ray observations using the broken power-law model. We found $E_b = (2.01\pm0.22)$ keV. In the case of the log-parabola model fitted the comparison of different $N_H$ values favours the $N_H$ value taken from Willingale et al. (2013) survey.

In previous studies the curvature of the spectrum obtained with BeppoSAX observations was also preferred by Tagliaferri et al. (2000) and Donato et al. (2005). Donato et al. (2005) claim that the break energy is equal to $E_b = 3.09^{+1.33}_{-1.15}$ keV or $E_b = 2.70^{+0.47}_{-1.33}$ keV. Tagliaferri et al. (2000) has found similar values of $E_b$.

MS 1221.8+2452: The blazar in the X-ray regime is described with the log-parabola model with any of $N_H$ values tested and with the power-law model with free value of the Galactic absorption column density. For the other cases $\chi^2_{red}$ is about 1.5, while for the preferable cases $\chi^2_{red} \sim 1.1$.

4C +21.35: Power-law and log-parabola fits result in $\chi^2_{red}$ of about 1.0 and $\sim 1.7$, respectively.

Negative values of a $\beta$ parameter in the case of the log-parabola model imply an up-turn of SED located in the X-ray range. The broken power-law fit to data placed the break energy at $(1.18 \pm 0.10)$ keV. The best description of the log-parabola fits is given with free $N_H$ value, but this is much smaller than the ones provided by Kalberla et al. (2005), Dickey & Lockman (1990) or Willingale et al. (2013). The latter discussed values of $N_H$ describe the spectrum with a comparable accuracy.

3C 279: The X-ray spectrum is well explained using the log-parabola model and different values of $N_H$ result in consistent $\chi^2_{red} \sim 1.1$. The power-law model can also be used for this source, but only with free $N_H$ value. Fits with the Galactic absorption values taken from the surveys results in $\chi^2_{red} \sim 1.3$. For the log-parabola model different values of $N_H$ tested result in very similar values of $\alpha$ and $\beta$ parameters.

In the previous studies Donato et al. (2005) found that BeppoSAX observations of 3C 279 can be characterised with the power-law and the broken power-law models, depending on the observation date. In the latter case the break energy point is in low energies $\sim 0.5-0.7$ keV.

PKS 1424+240: In the energy range of 0.3-10 keV the spectrum can be well characterized with the log-parabola model with all $N_H$ values tested and with the power-law model, but only with free $N_H$ value. In all the mentioned cases the spectral fitting results in $\chi^2_{red} \sim 1.0$. For the comparison the other power-law fits, with $N_H$ values provided by Kalberla et al. (2005), Dickey & Lockman (1990) or Willingale et al. (2013) result in $\chi^2_{red}$ of about 1.4-1.5. Acciari et al. (2010a) found single power-law model as preferable to describe X-ray spectrum of the blazar. Similar result found Aleksić et al. (2014a) for the Swift/XRT observations of PKS 1424+240.

H 1426+428: A log-parabola model provides $\chi^2_{red}$ value of about 1.2, while in the case of the power-law model the fitted $\chi^2_{red}$ is about 1.6-1.7. All $N_H$ values tested in the case of the
log-parabola model give comparable results regarding the spectral index and the curvature parameter.

The curved shape of the spectrum of the blazar is also suggested in previous studies for BeppoSAX, XMM-Newton and Swift/XRT observations by Massaro et al. (2008) and Tramacere et al. (2007), while Giommi et al. (2002) favours the power-law model as a description of the BeppoSAX observations.

PKS 1510−089: The Swift/XRT spectrum of this blazar is best described with either a power-law or a log-parabola fit. The favourable $N_H$ values are the ones provided by Kalberla et al. (2005) and free $N_H$ value. For the log-parabola model also the $N_H$ value taken from Dickey & Lockman (1990) gives satisfying result. The free $N_H$ values are smaller than the values provided in the quoted surveys. $\chi^2_{red}$ values of the preferred fits are close to 1.0.

Donato et al. (2005) found the broken power-law as the best description of BeppoSAX observations. Again, in this case, the break energy is found to be in the low energy part of the X-ray range i.e. $E_b = 1.41^{+1.22}_{-0.45}$ keV.

PG 1553+113: The X-ray spectrum can be well described using both a power-law and a log-parabola models, but in the first case only with the free $N_H$ value. In the case of the log-parabola models similar values of $\chi^2_{red}\sim1.2$ are obtained using different $N_H$. The log-parabola model the different values of $N_H$ result in very similar values of $\alpha$ and $\beta$ parameters. Massaro et al. (2008) and Tramacere et al. (2007) described the X-ray spectra with the curved log-parabola models. The object was also a target of studies by Donato et al. (2005), fitted the power-law and the broken power-law models, depending on the observation date. However Giommi et al. (2002) favour the log-parabola hypothesis, also for BeppoSAX monitoring. More recent multi-wavelength studies of the blazar confirmed preference of a convex curved model for Swift/XRT data (Alesić et al. 2014b).

1ES 1959+650: A For the case of the log-parabola model $\chi^2_{red}$ values are around 1.2-1.3, while in the case of the power-law model $\chi^2_{red}$ is about 1.3 for the case of free $N_H$ value and the one taken from survey by Willingale et al. (2013) and 2.0 in the other cases. In the case of the log-parabola fit with $N_H$ value from Willingale et al. (2013) the $\beta$ parameter is negative, which we do not find as a preferable description of the X-ray spectrum of this blazar, especially while the observations collected in the other wavelengths are considered.

Giommi et al. (2002); Donato et al. (2005); Tramacere et al. (2007) used the log-parabola model and the broken power-law one as preferred for X-ray spectrum of this blazar. In the recent multi-frequency studies of the source, including also Swift/XRT and RXTE-PCA data, the power-law model is found as a satisfactory description (Aliu et al. 2013 2014a).

PKS 2005−489: The X-ray spectrum can be well characterized using the log-parabola and the power-law models. Also all values of $N_H$ tested result in comparable values of $\chi^2_{red}\sim1.0$. All the spectral fits give very similar values of the fit parameters. The negative values of $\beta$ suggest a concave curvature, but the errors calculated for the parameter are large compared to the value. The curvature effect is caused by the high energy part of the spectrum, where only a few last spectral points rise.

In the previous works Donato et al. (2005) found the broken power-law as the best model to characterize BeppoSAX observations of PKS2005−489, while Giommi et al. (2002); Tramacere et al. (2007); Massaro et al. (2008) suggested a description of BeppoSAX, XMM-Newton and Swift/XRT observations with the log-parabola model. Several multi-wavelength campaigns targeting the source also included the X-ray observations with different instruments, both in the low and the high states of the blazar. In most of these cases soft X-ray observations are well described with the single power-law model (e.g. Sambruna et al. 1995; Perlman et al. 1999; Tagliaferri et al. 2001; Rector et al. 2002; H.E.S.S. Collaboration 2010; 2011b).

PKS 2155−304: For the blazar the X-ray spectrum is well fitted using the log-parabola model. Different values of $N_H$ tested result in comparable $\chi^2_{red}\sim1.1$, while in the case of the power-law model fitted $\chi^2_{red}\sim1.2$. Again, this is the case of blazar for which different values of $N_H$ tested, for the power-law as well as the log-parabola model result in very similar values of the $\alpha$, $\beta$, and $\Gamma$ parameters.

In the earlier studies Donato et al. (2005) found the curved log-parabola model as the best description of BeppoSAX observations. The same model was successfully used by Giommi et al. (2002); Tramacere et al. (2007); Massaro et al. (2008) for BeppoSAX, XMM-Newton and Swift/XRT observations. The studies of XMM-Newton observations of PKS 2155−304 in 2006 revealed a curved shape of the spectrum and an indication of both synchrotron and inverse Compton components revealed in data (Zhang 2008).

The results mentioned suggest that PKS 2155−304 can be a rare example of HBL type blazar for which possible up-turn point of SED is found in soft X-ray regime. However previous studies with BeppoSAX observations of the source were well described with the single power-law or the convex broken power-law model (e.g. Zhang et al. 1999; Chiappetti et al. 1999; Zhang et al. 2002). Also during the multi-wavelength studies targeting the low state of the blazar X-ray spectrum was well characterized with the broken power-law model (Aharonian et al. 2009). Detailed, longterm spectral studies, including observations of the blazar obtained during the period of 2005-2012 with XMM-Newton has been successfully described with the log-parabola model (Kapanadze et al. 2014).

BL Lacertae: The X-ray spectrum of this blazars can be well fitted with the power-law as well as with the log-parabola model, but in both cases with free value of the Galactic absorption parameter and the one provided by Willingale et al. (2013). In the case of the X-ray spectrum of BL Lacertae different values of $N_H$ tested, for the power-law as well as the log-parabola models, result in diametrically different values of the spectral and curvature parameters. Visual inspection of data suggests the curvature in the X-ray domain, but it is difficult to quantify, due to the high dispersion of data points in low energy part of the spectrum. For the preferable fits $\chi^2_{red}$’s about 1.1-1.2.

Previous studies on this blazer’s spectrum in the X-
ray energy band disentangle synchrotron and inverse Compton components in this range. [Tanihata et al. 2000] found that for the blazar in the energy range below 1 keV a soft and steep spectrum is dominating, in contrast to hard component otherwise. [Ravasio et al. 2002] reported two periods of observations of the blazar in 1999. In June the source has a concave spectrum with a very hard component above 5-6 keV, while in December data were well fitted with the power-law. [Donato et al. 2005] found the spectrum well described with the broken power-law model with the break energy $E_b = 0.45^{+0.43}_{-0.39}$ keV. Also, the observations of BL Lacertae with INTEGRAL/IBIS are also well described with the broken power-law model with $E_b = 1.71^{+0.07}_{-0.15}$ keV. [Raiteri et al. 2009] in the multi-wavelength studies including XMM-Newton observations of the source also unveiled a concave curvature in the X-ray regime. The curved model is also the preferable one for The BeppoSAX observations studied by [Massaro et al. 2008], while [Giommi et al. 2002] suggested the single power-law as the best description for BeppoSAX data.

B3 2247+381: The X-ray spectrum of this blazar is well characterized with the log-parabola model with any of $N_H$ values tested. In each of the mentioned cases $\chi^2_{\text{red}}$ is about 1.0. A good description of the spectrum is also given with the power-law model with free $N_H$ value and the one provided by [Willingale et al. 2013]. For the other $N_H$ values tested, the one provided by [Kalberla et al. 2005] and by Dickey & Lockman (1990), $\chi^2_{\text{red}}$ values are 1.6 and 1.3, respectively.

1ES 2344+514: The best description of the spectrum is given with the log-parabola model and a free Galactic absorption value as well as $N_H$ provided by [Kalberla et al. 2005] and Dickey & Lockman (1990). For these preferable cases $\chi^2_{\text{red}}$ is about 1.1. The log-parabola fit with $N_H$ from [Willingale et al. 2013] survey results in the largest value of $\chi^2_{\text{red}}$ of about 1.3 and negative value of the $\beta$ parameter. As in the case of 1ES 0414+009, the $\beta$ value is not consistent with the SED shape (see e.g. [Aleksić et al. 2013]). In the context of the power-law model a fit with a free value of the Galactic column density gives a satisfactory result.

Previous studies of the X-ray spectra obtained with Swift/XRT and BeppoSAX show that these data cover the synchrotron bump in its SED. The X-ray spectrum was usually well described with the power-law model (e.g. [Giommi et al. 2000] [Acciari et al. 2011] [Aleksić et al. 2013]). However a need for a curved model was found also for the case of BeppoSAX X-ray data by [Massaro et al. 2008]. It is also worth mentioning that 1ES 2344+514 exhibits strong spectral variability with the synchrotron peak shifting to higher energies during flares ([Giommi et al. 2000]). The synchrotron peak frequency during such events is at 10 keV or above, which classifies the source as the so-called extreme HBL.

5 BLAZERS WITH UPWARD-CURVED X-RAY SPECTRA

In the further studies we focus on five blazars for which a concave curvature of the spectrum suggests that both synchrotron and inverse Compton components are located in the X-ray regime. This gives a perfect opportunity to study spectral and temporal variability of both components contemporaneously.

In the first step the longterm background-subtracted light curves for each source were inspected (upper panels of Fig. 3). In each case the presented light curves show observations from 2005 up to October 2014 collected with Swift/XRT in the PC mode in the energy range of 0.3-10 keV. Each light curve is binned in observation-length intervals.

In order to separate synchrotron and inverse Compton components we define the upturn energy ($E_{\text{upt}}$) being identical to the break energy value taken from the broken power-law fit, which is given in Table 5. We define two energy bands for each source. The soft band in the energy range (0.3 keV, $E_{\text{upt}}$) and the hard energy band ($E_{\text{upt}}$, 10 keV). Note that $E_{\text{upt}}$ is kept constant for each source throughout the 10 years period. The variations in both bands and of the hardness ratio (HR), defined as the proportion of the count rate in the hard and the soft band, are shown in Fig. 3.

3C 66A: The light curve (see upper panel of Fig. 3) shows variability manifested mainly in one outburst in 2008. The flux changes are characterized by a fractional variability amplitude ($F_{\text{var}} = (67 \pm 2)\%$ with the uncertainty calculated following [Vaughan et al. 2003]). Except for this outburst (with a count rate of $0.7 \text{count/s}$) the source flux level observed in different epochs is about 0.1-0.2 counts/s. The soft and the hard X-ray light curves in the energy bands of 0.3-3.4 keV and 3.4-10 keV, respectively are shown in Fig. 3. The fractional variability amplitudes for the soft and hard bands are following: $F_{\text{var}} = (69 \pm 2)\%$ and $F_{\text{var}} = (56 \pm 1)\%$, respectively. The hardness ratio is characterized by a fractional variability amplitude of $F_{\text{var}} = (28 \pm 1)\%$. Hence, the most pronounced variability is observed in the soft energy band.

To investigate the spectral variability of 3C 66A in detail, spectra have been obtained during three intervals, shown in Fig. 3. The division takes into account the exposure for spectral analysis in each interval and the range of different flux levels for the source. The assumes a monotonous change of spectral properties with the total flux even if several distinct flares are coadded. In the first interval there are only two observations performed in 2005, but the second one has an exposure of 52 ks. For each of the selected intervals, data are fitted with the broken power-law model with the Galactic absorption ($N_H$ value taken from LAB survey), which describe the overall spectrum well. The spectral parameters are collected in Table 6. The plots presenting SEDs for all intervals are shown in Fig. 3. In Sect. 3 it was shown that the average spectrum is characterised by concave curvature and an upturn energy of about 3.4keV. This value is an average one and the soft and hard intervals selected in Fig. 3 do not reflect precisely the synchrotron and the inverse Compton components for all times. The concave shape of the spectrum is clearly visible in the first interval. For the other intervals the upturn is not visible and the spectrum in the energy band presents only a synchrotron component. Since the third epoch display the source at a fainter state compared to the first one, the absence of an upturn implies flux variability of the inverse Compton component.

Figure 4 presents the comparison of the hardness ratio and the total count rate. There is no clear trend between...
these quantities. The soft spectral state is observed in bright or faint, while the hard state of the source is for faint state.

**S5 0716+714**: The source, known for its variability, clearly manifests this feature in the longterm light curve presented in the upper panel of Fig. 11. The middle panels of Fig. 11 shows the hard and soft light curves, for which the energy bands are defined as 1.1-10 keV and 0.3-1.1 keV, respectively. The longterm variability is characterized by fractional variability amplitude for the total, soft and hard bands resulting in $F_{\text{var}} = (61 \pm 1)$%, $F_{\text{var}} = (75 \pm 1)$% and $F_{\text{var}} = (52 \pm 1)$%, respectively. For the comparison the hardness ratio light curve (see bottom panel in Fig. 11) results in $F_{\text{var}} = (22 \pm 2)$%. Then, the most prominent variability is observed in the soft energy range.

To study the spectral variability we divide the light curve into four intervals (see Fig. 11). The first interval includes only two observations, but the first one has the time exposure of 19 ks. Each of the spectrum, for selected intervals, can be well characterized with the broken power-law model with the Galactic absorption $N_H$ value from DL survey. The spectral parameters are collected in Table 6 and the corresponding plots are shown in Fig. 13. All the selected intervals have similar value of the break energy, between 0.9 and 1.4 keV. The overall the broken power-law fit to data results in the break energy of 1.1 keV. This indicates that division into the soft and the hard intervals with a good approximation reflects synchrotron and inverse Compton components. We also investigate the spectral variability in the context of flux variation. Hardness ratio - total count rate comparison, presented in Fig. 14, indicates behaviour similar to the one observed in the case of 3C66A. It is also worth mentioning that in the case of this source we do not see clear harder-when-brighter trend or the opposite softer-when-brighter one. While the anticorrelation of the hardness ratio and the flux count rate in the case of S5 0716+714 was previously reported in the X-ray regime by e.g. Foschini et al. (2006) and Ferrero et al. (2006). The values of the spectral indices indicate significant spectral variability of the synchrotron component, which is not observed in the case of the inverse Compton part of the spectrum.

**W Comae**: The observed count flux rate (see the upper panel of Fig. 11) changes in the range of 0.1-0.7 counts/s. The figure shows also the soft (0.3-2.0 keV) and the hard (2.0-10.0 keV) energy band light curve as well as the hardness ratio evolution. The longterm variability of the blazar can be characterized with fractional variability amplitude resulting in $F_{\text{var}} = (94 \pm 1)$%, $F_{\text{var}} = (69 \pm 2)$%, $F_{\text{var}} = (56 \pm 6)$%, and $F_{\text{var}} = (28 \pm 9)$% for the total, the soft, the hard and hardness ratio light curve respectively. These results show that the highest variability is observed in the energy range of 0.3-10 keV.

As in the case of previously discussed sources, separate intervals are distinguished to investigate spectral features in the different states. In the case of W Comae two intervals are considered representing the low (the second interval) and the elevated (the first interval) flux level (see Fig. 9). The data collected during both periods are fitted with the broken power-law model with the Galactic absorption $N_H$ taken from the survey provided by Willingale et al. (2013). The spectral fit parameters are collected in Table 6 while all corresponding plots are shown in Fig. 13. In both intervals the spectral shapes reveal a concave curvature. The selected intervals are characterized with different values of the break energy: 4.1 keV and 1.2 keV for the first and the second interval, respectively. It is worth reminding here that the crossing point in the broken power-law fit to all data is determined as 2.0 keV. Because of this fact the soft and the hard energy bands used for the light curves do not indicate clearly the synchrotron and inverse Compton components. The values of the spectral indices reveal larger spectral variability in the soft energy band. The comparison of the hardness ratio and the total count rate, presented in Fig. 14, exhibit similar behaviour as in the case of 3C66A and S5 0716+714.

**4C +21.35**: The light curve presenting the longterm variability of the blazar (see the upper panel of Fig. 12) shows smaller changes in the observed count rate than in the case of other blazars discussed here. The variability observed in the energy range of 0.3-10 keV can be described with fractional variability amplitude as high as $F_{\text{var}} = (39 \pm 1)$%. The soft and the hard energy bands, presented in the middle panels of Fig. 12, are defined as: 0.3-1.2 keV and 1.2-10 keV. The value of 1.2 keV is the break energy point found in the average spectrum of this blazar. To check whether the fractional variability amplitude depends on the energy band considered, this quantity has been also calculated for the soft and the hard energy bands resulting in: $F_{\text{var}} = (56 \pm 1)$% and $F_{\text{var}} = (31 \pm 1)$%, respectively. The bottom panel in Fig. 12 show hardness ratio light curve, which is characterized by $F_{\text{var}} = (23 \pm 1)$%.

Three intervals have been distinguished for detailed spectral studies. The spectral analysis has been repeated for each of the interval. Since in the case of set of all observations data are well described with broken power-law model with the Galactic absorption, here also this model has been used. For this case $N_H$ value taken from Willingale et al. (2013) survey is used. Reduced $\chi^2$ values show that this model works well also for shorter intervals. All the spectral parameters of the broken power-law fit and the corresponding plots are collected in Table 6 and shown in Fig. 13. For the intervals selected the broken power-law fit results in the break energy of value 1.0-1.2 keV. We can then conclude that the soft and the hard energy bands with a good approximation correspond to the synchrotron and the inverse Compton spectral components, respectively. The comparison of the hardness ratio and the total count rate, presented in Fig. 14 shows complex behaviour, with individual substructures and indication for hysteresis effects visible within each.

**BL Lacertae**: The light curve of BL Lacertae (see upper panel of Fig. 10) in the energy range of 0.3-10 keV shows significant variability exhibited in several outbursts. The longterm variability is characterized using fractional variability amplitude with the value of $F_{\text{var}} = (52 \pm 1)$%. As in the previous cases, we also consider the soft and the hard energy bands defined as 0.3-1.1 keV and 1.1-10.0 keV, respectively, as well as the hardness ratio. The variability in the soft and the hard energy ranges is then given by $F_{\text{var}} = (47 \pm 1)$% and $F_{\text{var}} = (58 \pm 1)$%, respectively. The variability amplitude is more pronounced in the higher-
energies. For the comparison the hardness ratio variability is quantified by \( F_{\text{HAR}} = (13 \pm 1)\% \).

To check if the crossing point, disentangling the synchrotron and the inverse Compton components, is shifting for the different flux states of the source, four intervals are distinguished (see the light curve in Fig. 11). Each of the intervals represents different the X-ray behaviour of BL Lacertae. Data in each interval are then fitted with the broken power-law model with the Galactic absorption \( N_H \) taken from the survey provided by [Willingale et al. (2013)]. The fit parameters are collected in Table 6 and the corresponding plots are shown in Fig. 13. Let us here remind that the broken power-law fit to all data results in the break energy of 1.1 keV. For the shorter intervals the break energy is oscillating between 1.1-1.2 keV. A clear upturn of the spectrum, disentangling two spectral components is visible in the case of the three intervals discussed.

Furthermore, there is no significant shift of the crossing point to the higher energies with the increasing flux, which is observed in the other blazars discussed. Hence, for this blazar the soft and hard energy bands in a good approximation correspond to the synchrotron and the inverse Compton components. The synchrotron component is then characterized by larger spectral variability comparing to the inverse Compton one. The hardness ratio seem to be correlated with the total count rate (see Fig. 14), which is not surprising in the case of HBL type blazars, but it is not a common feature of the IBL ones.

6 SUMMARY AND CONCLUSIONS

In this paper we study spectra of 29 TeV \( \gamma \)-ray emitting blazars including 22 HBL, 4 IBL type blazars, and 3 FSRQs observed with \textit{Swift}/XRT in the energy range of 0.3-10 keV.

The only one LBL blazar detected in TeV \( \gamma \)-ray regime, (AP Librae) is not part of the sample presented here. Since only TeV blazars are included in the sample and HBL type objects are known to be the brightest in this regime, three groups of blazars included are not distributed uniformly.

The spectra studied are averaged, which means that they include observations in the low and the high states, for data collected since the mission start up to October 2014. We focus only on the PC mode observations, which implies that the highest outbursts are not included in the averaged spectra. This is the first spectral survey including 10 years of observations of TeV emitting blazars collected with \textit{Swift}/XRT.

We conclude that the most of the spectra are well described using the curved log-parabola model. Only in a few cases we get better characteristics with the power-law model. These are 1ES 1101−232, Mrk 180, and PKS 2005−489. There are also a few cases of objects for which we got acceptable power-law fit only if the free \( N_H \) value is used. These are mainly cases for which free value of the Galactic absorption is much higher than the ones provided in the discussed surveys.

The curved log-parabola model has been used to describe the shape of radio-optical blazars spectra for the first time by [Landau et al. (1986)]. The first X-ray studies involving the log-parabola as the best model for spectral fits have been performed by [Giommi et al. (2002)] who found this model as the preferable one for 50% of blazars studied. Also [Massaro et al. (2004a), Tramacere et al. (2007), Massaro et al. (2008)] successfully used this model in their X-ray spectral studies.

The observed convex curvature in the X-ray spectra is likely to result from a single accelerated particle distribution (e.g. [Massaro et al. (2004a)]. The concave curvature observed may be caused by the fact that the X-ray range is a place, where synchrotron and inverse Compton components meet and the curvature is a consequence of the spectral upturn. In the latter case the X-ray observations enable simultaneous study of the low and the high energy ends of the particle distribution function.

Different values of \( N_H \) tested do not allow us to find one universal set. On the other hand we cannot conclude that any of mentioned \( N_H \) surveys can be used in each case to obtain good fit. But we can then summarize that each case should be treated separately, often including wider view on spectral features also in different wavelengths, see an example of two blazars presented in Fig. 15, where the \textit{Swift}/XRT observations are combined with the \textit{Swift}/BAT ones.

Furthermore, our studies has shown that the Galactic column density value influence the overall spectral fit. In general larger \( N_H \) values result in softer spectral index, i.e. larger value of \( \Gamma \) or \( \alpha \) parameter in the power-law and the log-parabola model, respectively. Also in most cases for the log-parabola model fitted the curvature parameter is larger for smaller \( N_H \) values. Hence, we can summarize that the choice has significant influence on the X-ray spectral features. It is also worth mentioning that \( \chi^2_{\text{red}} \) is not a good indicator, which could be used to distinguish the most accurate value of the Galactic column density. Let us here remind the example of 1ES 0033+595, for which very different values of \( N_H \) result in the significantly different spectral fit parameters and very similar values of \( \chi^2_{\text{red}} \) (see Fig. 6 and 8, and Table 3 and 4 in the online material).

In the mentioned case too small value of \( N_H \) e.g. the one taken from LAB survey result in the spectral shape with the artificial bump which cannot be easily explained. Very similar situation take place for the cases of blazars such like 1ES 0502+675, 1ES 0647+250 or 1ES 1959+650.

The log-parabola model is described by the \( \alpha \) parameter, which corresponds to the spectral index and \( \beta \) one, which characterize the spectral curvature. We found the spectral indices \( \alpha \) in the range of 1.4-2.6.

The performed spectral studies of 29 \( \gamma \)-ray emitting blazars allow us to distinguish only 5 blazars for which the concave spectral shape indicates that in the X-ray regime synchrotron and inverse Compton components meet. Since the spectral upturn is expected in all blazar SEDs and we focused on the energy range of one magnitude, we then conclude that the spectral upturns are distributed in the broad range of energies. The second part of the paper includes detailed temporal and spectral studies focused on 5 sources for which concave shape of the spectrum indicates that the synchrotron and the inverse Compton components meet in the X-ray regime. The mentioned sources are: 4C +21.35, S5 0716+714, BL Lacertae, 3C 66A, and W Comae. For each of the objects the preferable model to describe the spectral shape is the log-parabola with a concave curvature. For these
five blazars with the upturn, we fit spectra with the broken power-law model, which helps us to find the crossing point for the average spectrum, disentangling the synchrotron and the inverse Compton components. For all sources the upturn point is clearly visible in the averaged spectrum for the dataset including all data analysed. But for the case of shorter time intervals synchrotron and inverse Compton components are not always visible. For example 3C 66A for A and B intervals two components are clearly visible, while for the case of the third distinguished interval, the spectral shape reveals only the synchrotron part of the spectrum. It is also worth underlining that the upward curvature was previously reported for 3S 0716+714 (Cappi et al. 1994; Giommi et al. 1999; Tagliaferri et al. 2003; Donato et al. 2005; Ferrero et al. 2006), BL Lacertae (Tanihata et al. 2000; Ravasio et al. 2002; Donato et al. 2005; 3C 66A (Donato et al. 2005), and W Comae (Tagliaferri et al. 2000; Donato et al. 2005), while this is the first case when the upturn between the synchrotron and the inverse Compton component is found for 4C +21.35. Using Swift/XRT observations of blazars we found five objects with the spectral upturn. Also, there are objects for which single Swift/XRT observations do not reveal this feature, but joint spectrum, that include Swift/XRT and Swift/BAT data show such an upturn. But since Swift/BAT spectra are longterm-averaged it is difficult to quantify the number of such objects. As an example Fig. 15 show joint fits for PKS 0548-322 and PKS 2005-489.

The longterm variability of those five blazars has been characterized with fractional variability amplitude. This quantity is also calculated for the distinguished the soft and the hard energy bands as well as for the hardness ratio evolution. The soft and the hard energy band corresponds to the synchrotron and the inverse Compton components in the average spectral fit. For 4C +21.35, 3S 0716+714, 3C 66A, and W Comae the largest value of $F_{\text{var}}$ is obtained for the soft energy range, while the lowest variability is observed for the hardness ratio light curve. Only for BL Lacertae the largest value of $F_{\text{var}}$ is for the hard energy range.

We also investigate the spectral variability by dividing the light curves into shorter intervals and performing spectral analysis for smaller data sets. In this case only the broken power-law model with the Galactic absorption value taken from LAB survey is tested. In the case of 3S 0716+714, 4C +21.35 and BL Lacertae the energy break value are consistent within errors with the value obtained for the average spectrum. Hence, we conclude that the distinguished soft and the hard energy bands corresponds to the synchrotron and the inverse Compton components, respectively. In the case of 3C 66A, and W Comae the break energy values for the short intervals and the average spectrum are different, so the soft and the hard bands can not be unambiguously associated with the synchrotron and the inverse Compton components. Furthermore the comparison of the spectral indices for the broken power-law fit for the shorter intervals revealed significant variability in the soft energy range, while in the hard one the variability is not noticed in the case of 3C 66A.

We also compared the hardness ratio, calculated as a ratio of count rates in the hard and the soft energy bands, with the total intensity. This comparison revealed different behaviours of in HR-total intensity diagrams. For three of studied blazars, namely 3C 66A, W Comae and 3S 0716+714 for the soft spectrum (smaller values of HR) total intensity of the sources changes in the whole range of brightness. While when the source is faint, different values of HR can be observed. Such a behaviour suggests that in the faint state of the source the influence of the inverse Compton component is more significant. For BL Lacertae HR-total intensity diagram exhibit harder-when-brighter trend. Such a behaviour is a common feature for HBL type blazars (e.g. Pian et al. 1998; Zhang et al. 2003; 2006; H.E.S.S. Collaboration 2012), while IBL and LBL ones often exhibits softer-when-brighter pattern (e.g. Giommi et al. 1999; Ravasio et al. 2002; Ferrero et al. 2006). The case of 4C 21.35 is the most complex one with individual substructures and an indication for hysteresis effects visible within each. Such a hysteresis trend visible in HR-flux diagram can be related to the changes of the acceleration and cooling time scales (Kirk et al. 1998).
Figure 1. The X-ray spectral energy distributions of 29 selected blazars sorted by increasing flux density. The names of the sources are given in the upper part of each panel. Four log-parabola spectral models with different values of $N_H$ are presented in different colours: red – $N_H$ taken from the LAB survey (Kalberla et al. 2005), blue – $N_H$ value taken from Dickey & Lockman (1990), magenta – $N_H$ value taken from Willingale et al. (2013) and green – free $N_H$ value. Data (grey points) presented in the figure are those fitted with the log-parabola model with the Galactic absorption value taken from LAB survey.
Figure 2. The X-ray spectral energy distributions of 29 selected blazars sorted by increasing flux density. The names of the sources are given in the upper part of each panel. Four power-law models using different values of $N_H$ are presented using different colours: red – $N_H$ taken from the LAB survey (Kalberla et al. 2005), blue – $N_H$ value taken from Dickey & Lockman (1990), magenta – $N_H$ value taken from Willingale et al. (2013) and green – free $N_H$ value. Data (grey points) presented in the figure are those fitted with the power-law model with the Galactic absorption value taken from LAB survey. The figure is available in the online material only.

Figure 3. The X-ray spectra fitted with the log-parabola model with the Galactic absorption value taken from LAB survey and the ratios (data points divided by the folded model). The plots present spectra for: 1ES 0033+595, RGB J0136+391, 3C 66A, 1ES 0229+200, PKS 0447-437, 1ES 0502+675. The name of each object is also given in the upper right corner of each plot.

Figure 4. The X-ray spectra fitted with the log-parabola model with the Galactic absorption value taken from LAB survey and the ratios (data points divided by the folded model). The following plots present spectra for: PKS 0548-322, 1ES 0647+250, S5 0716+714, 1ES 0806+524, 1ES 1011+496, 1ES 1101-232. The name of each object is also given in the upper right corner of each plot.

Figure 5. The X-ray spectra fitted with the log-parabola model with the Galactic absorption value taken from LAB survey and the ratios (data points divided by the folded model). The following plots present spectra for: Mrk 180, RX J1136.5+6737, 1ES 1218+304, W Comae, MS 1221.8+2452, 4C 21.35. The name of each object is also given in the upper right corner of each plot.

Figure 6. The X-ray spectra fitted with the log-parabola model with the Galactic absorption value taken from LAB survey and the ratios (data points divided by the folded model). The following plots present spectra for: 3C 279, PKS 1424+240, H 1426+428, PKS 1510-089, PG 1553+113, 1ES 1959+650. The name of each object is also given in the upper right corner of each plot.

Figure 7. The X-ray spectra fitted with the log-parabola model with the Galactic absorption value taken from LAB survey and the ratios (data points divided by the folded model). The following plots present spectra for: PKS 2005-489, PKS 2155-304, BL Lacertae, B3 2247+381, 1ES 2344+514. The name of each object is also given in the upper right corner of each plot.
Figure 13. Spectral energy distributions for spectral fits with broken power-law models during periods defined in Fig. 8-12 for 3C 66A, S5 0716+714, W Comae, 4C 21.35 and BL Lacertae. While both spectral components change in slope and flux normalization, the upturn energy ($E_{\text{upt}}$) does not display variations.
Figure 14. The comparison of the flux (total count rate) and the hardness ratio for 3C 66A, W Comae, BL Lacertae, S5 0716+714 and 4C 21.35. The soft and hard bands are chosen as described in Sect. 5 and presented in Fig. 8-12. The colour of a given data point indicates the time of a given measurement. The earliest observations are denoted by dark blue symbols and the most recent ones depicted in red, with the rainbow colour scale normalized to the entire span of the Swift/XRT observations of a given blazar. The same colour coding is used in Fig. 8-12.
Figure 15. The examples of joint spectral energy distributions including Swift/XRT and Swift/BAT data for PKS 0548-322 and PKS 2005-489. Each plot presents Swift/XRT data fitted with a log-parabola model, and the \( N_H \) value taken from LAB survey, and BAT data from the 70-Month Hard X-ray Survey (Baumgartner et al. 2013).
Figure 9. The longterm count rate and the hardness ratio light curve for W Comae. The following panels present: counts rate in energy range of 0.3-10 keV; the soft energy band of count flux (0.3-2.0 keV); the hard energy band of count rate (2.0-10 keV); the hardness ratio defined as ratio of hard and soft energy band count rate. The vertical dashed line indicates selected intervals discussed in Sect. 5. Different colours of data points indicate the time of a given measurement. The earliest pointings are denoted by dark blue symbols and the most recent ones depicted in red. The same colour coding is used in Fig. 14.

Figure 10. The longterm count rate and hardness ratio light curve for BL Lacertae. The following panels present: counts rate in energy range of 0.3-10 keV; the soft energy band of count flux (0.3-1.1 keV); the hard energy band of count rate (1.1-10 keV); the hardness ratio defined as ratio of hard and soft energy band count rate. The vertical dashed lines indicate selected intervals discussed in Sect. 5. Different colours of data points indicate the time of a given measurement. The earliest pointings are denoted by dark blue symbols and the most recent ones depicted in red. The same colour coding is used in Fig. 14.
Figure 11. The longterm count rate and hardness ratio light curve for S5 0716+714. The following panels present: counts rate in energy range of 0.3-10 keV; the soft energy band of count flux (0.3-1.1 keV); the hard energy band of count rate (1.1-10 keV); the hardness ratio defined as ratio of hard and soft energy band count rate. The vertical dashed lines indicate selected intervals discussed in Sect. 5. Different colours of data points indicate the time of a given measurement. The earliest pointings are denoted by dark blue symbols and the most recent ones depicted in red. The same colour coding is used in Fig. 13.

Figure 12. The longterm count rate and hardness ratio light curve for 4C 21.35. The following panels present: counts rate in energy range of 0.3-10 keV; the soft energy band of count flux (0.3-1.2 keV); the hard energy band of count rate (1.2-10 keV); the hardness ratio defined as ratio of hard and soft energy band count rate. The vertical dashed lines indicate selected intervals discussed in Sect. 5. Different colours of data points indicate the time of a given measurement. The earliest pointings are denoted by dark blue symbols and the most recent ones depicted in red. The same colour coding is used in Fig. 13.
Table 1. The summary of TeV blazars. (1) The object name, (2) the right ascension, (3) the declination, (4) the type of the blazar, (5) the redshift, (6) the integrated flux for Swift/XRT observations in PC mode in the energy range of 0.3-10 keV, (7) the exposure for Swift/XRT observations in PC mode in the energy range of 0.3-10 keV, (8) the product of (6) and (7), (9) the information if the blazar has been selected for the further detailed studies; selected objects are marked with + sign.

| Object          | RA           | DEC          | type  | redshift | PC flux 10^{-12} erg cm^{-2} s^{-1} | PC exposure ks | PC flux · exposure 10^{-11} erg cm^{-2} | notes |
|-----------------|--------------|--------------|-------|----------|----------------------------------|----------------|-----------------------------------|-------|
| SHBL J001355.9−185406 | 00 13 52.0 −18 53 29 | HBL | 0.095a | 12.30 | 14.4 | 1.77 | Not enough data in the PC mode to constrain spectral parameters. |
| KUV 00311−19382 | 00 33 34.2 −19 21 33 | HBL | 0.61b | 8.10 | 19.3 | 1.56 | |
| 1ES 0033+595 | 00 35 52.6 +59 50 05 | HBL | >0.24c | 109.90 | 15.2 | 16.70 | + |
| RGB J0136+391 | 01 36 32.5 +39 06 00 | HBL | Unknown | 23.80 | 18.8 | 4.47 | + |
| RGB J0152+0175 | 01 52 33.5 +01 46 40 | HBL | 0.08d | 6.58 | 27.1 | 1.78 | |
| 3C 66A | 02 22 41.6 +43 02 35 | IBL | 0.41e | 5.14 | 92.4 | 4.75 | + |
| 1ES 0229+007 | 02 32 53.2 +20 16 21 | HBL | 0.14f | 20.70 | 22.4 | 4.64 | + |
| PKS 0301−248 | 03 03 23.5 −24 07 36 | HBL | 0.2657g | 8.38 | 25.2 | 2.11 | |
| 1C 310 | 03 16 43.0 +41 19 29 | HBL | 0.0189h | 6.60 | 68.0 | 4.49 | |
| RBS 0413+58 | 03 19 47.0 +18 45 42 | HBL | 0.19i | 10.70 | 7.3 | 0.78 | |
| 1ES 0437−1211 | 04 37 23.0 −11 58 38 | HBL | 0.18j | 43.70 | 3.2 | 1.40 | |
| 1ES 0414+009 | 04 16 53.0 +01 05 20 | HBL | 0.28k | 18.30 | 6.2 | 1.13 | |
| PKS 0447−439 | 04 49 28.2 −43 50 12 | HBL | 0.10l | 24.60 | 50.5 | 12.42 | + |
| 1ES 0502+675 | 05 07 56.2 +67 37 24 | HBL | 0.34m | 49.60 | 39.9 | 19.79 | + |
| VER 0521+2111 | 05 21 45.0 +21 12 51 | IBL | 0.10n | 55.70 | 103.1 | 57.43 | + |
| PKS 0548−322 | 05 50 38.4 −32 16 12 | HBL | 0.06o | 31.80 | 71.4 | 22.71 | + |
| RX J0648.7+1516 | 06 48 45.6 +15 16 12 | HBL | 0.17p | 12.40 | 10.6 | 1.31 | |
| 1ES 0647+250 | 06 50 46.5 +25 03 03 | HBL | 0.45q | 31.80 | 71.4 | 22.71 | + |
| RGB J0710+591 | 07 10 26.4 +59 09 00 | HBL | 0.12r | 11.18 | 231.0 | 25.83 | + |
| S5 0716+714 | 07 21 53.4 +71 20 36 | IBL | 0.31s | 14.68 | 51.9 | 7.62 | + |
| 1ES 0806+524 | 08 09 59.0 +52 19 00 | HBL | 0.13t | 19.60 | 7.1 | 1.39 | |
| RBS 0723 | 08 47 12.9 +11 33 50 | HBL | 0.19u | 13.0 | 3.7 | 0.48 | |
| 1RXS J101015.9−311909 | 10 10 15.0 −31 18 18 | HBL | 0.14v | 19.60 | 7.1 | 1.39 | |
| S4 0954+654 | 09 58 47.0 +65 33 55 | FSRQ | 0.36w | 3.48 | 68.8 | 2.39 | |
| 1ES 1011+496 | 10 15 04.1 +49 26 01 | HBL | 0.21x | 34.30 | 58.5 | 20.07 | + |
| 1ES 1101−2326 | 11 03 36.5 −23 29 45 | HBL | 0.18y | 90.10 | 12.5 | 11.26 | + |
| Markarian 421 | 11 04 19.0 +38 11 41 | HBL | 0.03z | 37.90 | 50.7 | 19.22 | + |
| Markarian 180 | 11 36 26.4 +70 09 27 | HBL | 0.04aa | 37.90 | 50.7 | 19.22 | + |
| RX J1136.5+6737 | 11 36 30.1 +67 37 04 | HBL | 0.13bb | 20.70 | 21.0 | 4.35 | + |
| 1ES 1215+303 | 12 17 48.5 +30 06 06 | HBL | 0.23cc | 6.11 | 47.5 | 2.90 | |
| 1ES 1218+304 | 12 21 26.3 +30 11 29 | HBL | 0.18dd | 33.30 | 21.6 | 7.19 | + |
| W Comae | 12 21 31.7 +28 13 59 | IBL | 0.10ee | 3.13 | 166.3 | 5.21 | + |
| MS 1221.8+2452 | 12 24 24.2 +24 36 24 | HBL | 0.21ff | 15.60 | 28.2 | 4.40 | + |
| 4C +21.35 | 12 24 54.4 +21 22 46 | FSRQ | 0.47gg | 174.3 | 8.63 | + |
| S3 1227+255 | 12 30 14.1 +25 18 07 | IBL | 0.13hh | 15.03 | 595.6 | 89.52 | + |
| 3C 279 | 12 56 11.1 −05 47 22 | FSRQ | 0.53ii | 15.03 | 595.6 | 89.52 | + |
| 1ES 1312−423 | 13 14 58.5 −42 35 49 | HBL | 0.10jj | 28.20 | 4.8 | 1.35 | + |
| PKS 1424+240 | 14 27 00.0 +24 47 40 | HBL | 0.39kk | 9.03 | 49.8 | 4.50 | + |
| H 1426+428 | 14 28 32.6 +42 40 21 | HBL | 0.12ll | 59.20 | 123.6 | 73.17 | + |
| 1ES 1440+122 | 14 42 48.3 +12 00 40 | HBL | 0.16mm | 19.20 | 7.6 | 1.46 | + |
| PKS 1441+251 | 14 43 56.9 +25 01 44 | FSRQ | 0.93nn | 0.55 | 3.7 | 0.02 | + |
| (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| PKS 1510−089 | 15 12 52.2 | −09 06 21 | FSRQ | 0.360<sup>a</sup> | 10.51 | 362.9 | 38.05 | + |
| AP Librae | 15 17 41.8 | −24 22 19 | LBL | 0.049<sup>c</sup> | 6.36 | 32.7 | 2.08 | |
| PG 1553+113 | 15 55 44.7 | +11 11 41 | HBL | >0.62<sup>a</sup> | 43.70 | 86.5 | 37.80 | + |
| Markarian 504 | 16 53 52.2 | +39 45 37 | HBL | 0.037<sup>e</sup> | 0.00 | 0.00 | 0.0 | 0.0 |
| H 1722+119 | 17 25 04.3 | +11 52 15 | HBL | 0.018<sup>b</sup> | 10.65 | 2.7 | 0.29 | |
| 1ES 1727+502 | 17 28 18.6 | +50 13 10 | HBL | 0.055<sup>ab</sup> | 16.30 | 5.5 | 0.90 | |
| 1ES 1741+196 | 17 43 57.8 | +19 35 09 | HBL | 0.083<sup>ae</sup> | 11.70 | 18.8 | 2.20 | |
| HESS J1943+214 | 19 43 55.0 | +21 18 08 | HBL | >0.14<sup>d</sup> | 20.60 | 13.7 | 2.82 | |
| 1ES 1959+650 | 19 59 59.8 | +65 08 55 | HBL | 0.047<sup>c</sup> | 270.00 | 30.2 | 81.54 | + |
| MAGIC J2001+435 | 20 01 13.5 | +43 53 02 | IBL | <0.2<sup>ne</sup> | 2.11 | 62.2 | 1.31 | |
| PKS 2005−489 | 20 09 27.0 | −48 49 52 | HBL | 0.071<sup>ab</sup> | 31.00 | 50.1 | 15.53 | + |
| PKS 2155−304 | 21 58 52.7 | −30 13 18 | HBL | 0.116<sup>a</sup> | 97.10 | 89.8 | 87.20 | + |
| BL Lacertae | 22 02 43.3 | +42 16 40 | IBL | 0.069<sup>c</sup> | 14.15 | 365.6 | 51.73 | + |
| B3 2247+381 | 22 50 06.6 | +38 25 58 | HBL | 0.119<sup>ac</sup> | 10.60 | 42.3 | 4.48 | + |
| RGB J2243+203 | 22 43 54.7 | +20 21 04 | HBL | Unknown | 4.94 | 9.5 | 0.47 | |
| 1ES 2344+514 | 23 47 04.9 | +51 42 17 | HBL | 0.044<sup>f</sup> | 20.38 | 143.9 | 29.33 | + |
| H 2356−309 | 23 59 09.4 | −30 37 22 | HBL | 0.165<sup>ag</sup> | 5.68 | 17.1 | 0.97 | |

**TeV detection references:**

- [H.E.S.S. Collaboration](2013a), [Becherini et al.](2012), [Aleksić et al.](2015), [Mazin & MAGIC Collaboration](2012), [Aharonian et al.](2008), [Aliu et al.](2009), [Aharonian et al.](2007a), [H.E.S.S. Collaboration](2013c), [Aleksić et al.](2010), [Aliu et al.](2012), [Aharonian et al.](2007b), [H.E.S.S. Collaboration](2012), [Aharonian et al.](2013b), [Wystan Benbow for the VERITAS](2011), [Archambault et al.](2013), [Aharonian et al.](2010), [Aliu et al.](2011), [De Lotto & Magic Collaboration](2012), [Aharonian et al.](2010b), [Anderhub et al.](2009), [Acciari et al.](2009), [Mirzoyan](2014b), [H.E.S.S. Collaboration](2012), [Mirzoyan](2015), [Albert et al.](2007a), [Aharonian et al.](2007d), [Punch et al.](1992), [Albert et al.](2006b), [Mirzoyan](2014a), [Aleksić et al.](2012a), [Albert et al.](2006a), [Acciari et al.](2008), [Cortina](2013b), [Aleksić et al.](2011), [Mukherjee](2015a), [Errando et al.](2008), [H.E.S.S. Collaboration](2013), [Acciari et al.](2010a), [Horan et al.](2002), [Mukherjee](2015b), [H.E.S.S. Collaboration](2013), [H. E. S. S. Collaboration](2014), [Aharonian et al.](2006b), [Quinn et al.](1996), [Cortina](2013a), [Aleksić et al.](2014c), [Berger](2011), [H.E.S.S. Collaboration](2011a), [Nishiyama](1999), [Mariotti](2010), [Aharonian et al.](2005), [Chadwick et al.](1999), [Albert et al.](2007b), [Aleksić et al.](2012b), [Holder](2014), [Cataneo et al.](1998), [Aharonian et al.](2006a).  

**Redshift references:**  
- Jones et al. (2009), [Pita et al.](2014), [Sharufatti et al.](2005), [Rines et al.](2003), [Furniss et al.](2013), [Woo et al.](2005), [Falco et al.](1999), [Donato et al.](2001), [Liu & Zhang](2002), [Craig & Fruscione](1997), [Falomo & Kottlowski](1999), [Shaw et al.](2013), [Patruno et al.](2002), [Massaro et al.](2009), [Rector et al.](2003), [Abazajian et al.](2009), [Giovannini et al.](2005), [Snellen et al.](2002), [Albert et al.](2007c), [Lavaux & Hudson](2011), [Villforth et al.](2000), [Rines et al.](2005), [Bealey et al.](2008), [Véron-Cetty & Véron](2010), [Fey et al.](2004), [Shaw et al.](2012), [Aliu et al.](2014b), [Urry et al.](2000), [Laurent-Muehleisen et al.](1999), [Cerruti](2011), [Berger et al.](2011), [Ganguly et al.](2013), [Colless et al.](2001).
Table 2. The comparison of the Galactic column density values. (1) The object name, (2)-(5) the $N_H$ values provided by [Kalberla et al. (2005), Dickey & Lockman (1990) Willingale et al. (2013)], respectively, (6)-(8) the free $N_H$ value obtained with the log-parabola, the power-law and the broken power-law model fitted. The table is available in the online material only.

| Object         | $N_{LAB}^{H}$ [10$^{20}$ cm$^{-2}$] | $N_{DL}^{H}$ [10$^{20}$ cm$^{-2}$] | $N_{H2}$ [10$^{20}$ cm$^{-2}$] | $N_{Will}^{H}$ [10$^{20}$ cm$^{-2}$] | $N_{LP,\text{free}}^{H}$ [10$^{20}$ cm$^{-2}$] | $N_{PL,\text{free}}^{H}$ [10$^{20}$ cm$^{-2}$] | $N_{BP,\text{free}}^{H}$ [10$^{20}$ cm$^{-2}$] |
|----------------|----------------------------------|----------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|
| SHBL J001355.9−185406 | 2.13                             | 2.09                             | 0.17                            | 2.30                            |                                 |                                 |                                 |
| KUV 00311−1938   | 1.67                             | 1.59                             | 0.10                            | 1.77                            |                                 |                                 |                                 |
| 1ES 0033+595     | 41.80                            | 42.70                            | 14.40                           | 56.20                           | 59.36±0.42                      | 68.80±0.19                      |
| RGB J0136+391    | 6.00                             | 5.96                             | 1.30                            | 7.30                            | 12.0±1.5                        | 11.10±0.53                      |
| RGB J0152+017    | 2.68                             | 2.89                             | 0.23                            | 2.91                            |                                 |                                 |                                 |
| ...             | ...                              | ...                              | ...                             | ...                             | ...                             | ...                             | ...                             |
**Table 3.** Fit parameters for the log-parabola fits. (1) The object name, (2) source of $N_H$ value, (3)-(5) the $\alpha$, $\beta$ parameters and the normalization for the log-parabola fit defined in Sect. 3 (6) the reduced $\chi^2$ value and the number of degrees of freedom.

| Object       | $N_H$ | $\alpha$ | $\beta$ | $N_L$ | $\chi^2_{red}$/nd.o.f |
|--------------|-------|----------|---------|-------|------------------------|
|              | (1)   | (2)      | (3)     | (4)   | (5)                    |
| 1ES0033+595  | LAB   | 0.93±0.05| 0.66±0.07| 2.27±0.044 | 1.048/366               |
|             | DL    | 0.97±0.05| 0.93±0.07| 2.32±0.045 | 1.043/366               |
|              | Will  | 1.49±0.05| 0.47±0.07| 3.20±0.065 | 0.999/366               |
|              | free  | 1.60±0.16| 0.36±0.15| 3.44±0.338 | 1.001/365               |
| RGB0136+391  | LAB   | 2.07±0.02| 0.41±0.04| 0.718±0.008 | 0.922/259               |
|             | DL    | 2.07±0.02| 0.41±0.04| 0.717±0.008 | 0.924/259               |
|              | Will  | 2.16±0.02| 0.30±0.04| 0.744±0.008 | 0.900/259               |
|              | free  | 2.47±0.10| −0.07±0.12| 0.848±0.036 | 0.846/258               |
| 3C66A        | LAB   | 2.45±0.02| −0.19±0.04| 0.136±0.002 | 0.899/261               |
|             | DL    | 2.53±0.02| −0.29±0.05| 0.140±0.002 | 0.960/261               |
|              | Will  | 2.60±0.02| −0.37±0.04| 0.143±0.002 | 0.943/261               |
|              | free  | 2.76±0.08| −0.57±0.10| 0.153±0.005 | 0.929/260               |
| 1ES0229+200  | LAB   | 1.41±0.03| 0.38±0.05| 0.381±0.006 | 1.162/265               |
|             | DL    | 1.48±0.03| 0.30±0.05| 0.384±0.006 | 1.164/265               |
|              | Will  | 1.63±0.03| 0.14±0.05| 0.424±0.006 | 1.178/265               |
|              | free  | 1.40±0.12| 0.39±0.14| 0.379±0.022 | 1.166/264               |
| PKS0447−439  | LAB   | 2.49±0.01| 0.27±0.03| 0.654±0.006 | 1.177/273               |
|             | DL    | 2.55±0.01| 0.19±0.03| 0.697±0.006 | 1.154/273               |
|              | Will  | 2.49±0.01| 0.27±0.03| 0.657±0.006 | 1.175/273               |
|              | free  | 2.61±0.04| 0.10±0.07| 0.683±0.011 | 1.151/272               |
| 1ES0502+675  | LAB   | 1.89±0.02| 0.51±0.03| 1.315±0.011 | 1.104/348               |
|             | DL    | 1.90±0.02| 0.49±0.03| 1.322±0.011 | 1.110/348               |
|              | Will  | 2.21±0.02| 0.13±0.03| 1.517±0.012 | 1.032/348               |
|              | free  | 2.28±0.08| 0.06±0.10| 1.564±0.060 | 1.033/347               |
| PKS0548−322  | LAB   | 1.73±0.01| 0.17±0.02| 1.028±0.006 | 0.956/529               |
|             | DL    | 1.71±0.01| 0.20±0.02| 1.016±0.006 | 0.955/529               |
|              | Will  | 1.75±0.01| 0.15±0.02| 1.037±0.006 | 0.959/529               |
|              | free  | 1.70±0.04| 0.21±0.04| 1.015±0.016 | 0.957/528               |
| 1ES0647+250  | LAB   | 2.01±0.12| 0.45±0.03| 0.966±0.006 | 1.139/426               |
|             | DL    | 2.07±0.01| 0.38±0.03| 0.992±0.006 | 1.128/426               |
|              | Will  | 2.26±0.01| 0.17±0.03| 1.079±0.006 | 1.128/426               |
|              | free  | 2.16±0.06| 0.27±0.05| 1.035±0.003 | 1.125/425               |
| S50716+714   | LAB   | 2.07±0.01| −0.15±0.02| 0.116±0.001 | 1.029/434               |
|             | DL    | 2.11±0.01| −0.20±0.02| 0.230±0.002 | 1.024/434               |
|              | Will  | 2.10±0.01| −0.19±0.02| 0.230±0.002 | 1.025/434               |
|              | free  | 2.12±0.04| −0.22±0.05| 0.231±0.004 | 1.026/433               |
| 1ES0806+524  | LAB   | 2.37±0.01| 0.29±0.03| 0.414±0.003 | 0.994/284               |
|             | DL    | 2.39±0.01| 0.27±0.03| 0.418±0.003 | 0.990/284               |
|              | Will  | 2.42±0.01| 0.23±0.03| 0.422±0.004 | 0.985/284               |
|              | free  | 2.46±0.06| 0.18±0.08| 0.429±0.008 | 0.987/283               |
| 1ES1011+496  | LAB   | 2.25±0.01| 0.24±0.02| 0.938±0.006 | 1.268/360               |
|             | DL    | 2.24±0.01| 0.24±0.02| 0.937±0.006 | 1.269/360               |
|              | Will  | 2.25±0.01| 0.23±0.02| 0.938±0.006 | 1.267/360               |
|              | free  | 2.32±0.04| 0.15±0.05| 0.961±0.013 | 1.260/359               |
| 1ES1101−232  | LAB   | 2.02±0.02| 0.11±0.04| 1.910±0.022 | 1.034/269               |
|             | DL    | 2.03±0.02| 0.10±0.04| 1.916±0.022 | 1.035/269               |
|              | Will  | 2.11±0.02| 0.23±0.04| 1.987±0.023 | 1.053/269               |
|              | free  | 1.89±0.08| 0.25±0.10| 1.812±0.061 | 1.028/268               |
|          | (1)     | (2)     | (3)     | (4)     | (5)     | (6)     |
|----------|---------|---------|---------|---------|---------|---------|
| **Mrk 180** | LAB     | 2.09±0.01 | 0.25±0.03 | 0.848±0.006 | 1.012/339 |
|          | DL      | 2.11±0.01 | 0.23±0.03 | 0.854±0.006 | 1.005/339 |
|          | Will    | 2.10±0.01 | 0.25±0.03 | 0.850±0.006 | 1.011/339 |
|          | free    | 2.21±0.04 | 0.11±0.06 | 0.885±0.015 | 0.992/338 |
| **RX J1136.5+6737** | LAB     | 1.65±0.02 | 0.23±0.04 | 0.417±0.005 | 1.041/271 |
|          | DL      | 1.68±0.02 | 0.21±0.04 | 0.421±0.005 | 1.040/271 |
|          | Will    | 1.66±0.02 | 0.23±0.04 | 0.418±0.004 | 1.041/271 |
|          | free    | 1.71±0.08 | 0.17±0.10 | 0.427±0.014 | 1.043/270 |
| **1ES 1218+304** | LAB     | 2.04±0.02 | 0.13±0.04 | 0.927±0.001 | 1.198/287 |
|          | DL      | 2.02±0.02 | 0.15±0.04 | 0.921±0.001 | 1.195/287 |
|          | Will    | 2.05±0.02 | 0.12±0.04 | 0.930±0.001 | 1.199/287 |
|          | free    | 1.96±0.06 | 0.22±0.08 | 0.902±0.022 | 1.196/286 |
| **W Comae** | LAB     | 2.44±0.01 | −0.24±0.04 | 0.065±0.001 | 1.015/253 |
|          | DL      | 2.43±0.01 | −0.21±0.04 | 0.065±0.001 | 1.042/253 |
|          | Will    | 2.45±0.01 | −0.25±0.04 | 0.065±0.001 | 1.010/253 |
|          | free    | 2.63±0.06 | −0.48±0.08 | 0.070±0.002 | 0.968/252 |
| **MS 1221.8+2452** | LAB     | 2.18±0.02 | 0.39±0.04 | 0.395±0.005 | 1.143/240 |
|          | DL      | 2.18±0.02 | 0.39±0.04 | 0.396±0.004 | 1.143/240 |
|          | Will    | 2.19±0.02 | 0.38±0.04 | 0.397±0.005 | 1.139/240 |
|          | free    | 2.38±0.07 | 0.13±0.10 | 0.426±0.012 | 1.110/239 |
| **4C +21.35** | LAB     | 1.87±0.01 | −0.48±0.03 | 0.064±0.001 | 1.032/374 |
|          | DL      | 1.88±0.01 | −0.49±0.03 | 0.064±0.001 | 1.035/374 |
|          | Will    | 1.88±0.01 | −0.49±0.03 | 0.064±0.001 | 1.036/374 |
|          | free    | 1.75±0.05 | −0.35±0.06 | 0.061±0.001 | 1.018/373 |
| **3C 279** | LAB     | 1.48±0.01 | 0.16±0.02 | 0.245±0.001 | 1.108/607 |
|          | DL      | 1.49±0.01 | 0.14±0.02 | 0.246±0.001 | 1.110/607 |
|          | Will    | 1.49±0.01 | 0.14±0.02 | 0.246±0.001 | 1.108/607 |
|          | free    | 1.45±0.03 | 0.19±0.04 | 0.242±0.003 | 1.108/606 |
| **PKS 1424+240** | LAB     | 2.48±0.01 | 0.34±0.03 | 0.261±0.002 | 1.081/267 |
|          | DL      | 2.47±0.01 | 0.36±0.03 | 0.260±0.003 | 1.093/267 |
|          | Will    | 2.51±0.01 | 0.30±0.03 | 0.264±0.002 | 1.059/267 |
|          | free    | 2.76±0.05 | −0.04±0.07 | 0.288±0.006 | 0.968/266 |
| **H 1426+428** | LAB     | 1.84±0.01 | 0.10±0.01 | 1.423±0.006 | 1.245/583 |
|          | DL      | 1.86±0.01 | 0.18±0.01 | 1.434±0.006 | 1.246/583 |
|          | Will    | 1.84±0.01 | 0.20±0.01 | 1.424±0.006 | 1.245/583 |
|          | free    | 1.84±0.02 | 0.19±0.03 | 1.425±0.014 | 1.247/582 |
| **PKS 1510−089** | LAB     | 1.39±0.01 | −0.10±0.02 | 0.107±0.001 | 1.046/660 |
|          | DL      | 1.44±0.01 | −0.15±0.02 | 0.110±0.001 | 1.061/660 |
|          | Will    | 1.54±0.01 | −0.24±0.02 | 0.115±0.001 | 1.103/660 |
|          | free    | 1.28±0.04 | 0.01±0.04 | 0.101±0.002 | 1.033/659 |
| **PG 1553+113** | LAB     | 2.25±0.01 | 0.13±0.02 | 1.046±0.006 | 1.299/432 |
|          | DL      | 2.25±0.01 | 0.13±0.02 | 1.046±0.006 | 1.298/432 |
|          | Will    | 2.30±0.01 | 0.07±0.02 | 1.065±0.006 | 1.288/432 |
|          | free    | 2.33±0.03 | 0.03±0.05 | 1.076±0.015 | 1.290/431 |
| **1ES 1959+650** | LAB     | 1.91±0.01 | 0.40±0.02 | 7.301±0.042 | 1.263/466 |
|          | DL      | 1.94±0.01 | 0.36±0.02 | 7.400±0.042 | 1.230/466 |
|          | Will    | 2.29±0.01 | −0.01±0.02 | 8.669±0.049 | 1.331/466 |
|          | free    | 2.00±0.05 | 0.30±0.06 | 7.586±0.177 | 1.260/465 |

*Table 3 – continued*
| Source       | LAB   | DL    | Will  | free  |
|--------------|-------|-------|-------|-------|
| PKS 2005−489| 2.47±0.01 | −0.05±0.03 | 0.920±0.007 | 0.984/326 |
|              | 2.55±0.01 | −0.14±0.03 | 0.947±0.007 | 0.996/326 |
|              | 2.53±0.01 | −0.11±0.03 | 0.937±0.007 | 0.989/326 |
|              | 2.47±0.04 | −0.04±0.06 | 0.919±0.016 | 0.987/325 |
| PKS 2155−304| 2.38±0.02 | 0.23±0.05 | 3.834±0.050 | 1.151/208 |
|              | 2.39±0.02 | 0.21±0.05 | 3.852±0.051 | 1.149/208 |
|              | 2.38±0.02 | 0.22±0.05 | 3.844±0.051 | 1.150/208 |
|              | 2.45±0.07 | 0.13±0.11 | 3.926±0.106 | 1.151/207 |
| BL Lacertae | 1.23±0.02 | 0.48±0.02 | 0.266±0.002 | 1.164/615 |
|              | 1.40±0.02 | 0.31±0.02 | 0.292±0.002 | 1.122/615 |
|              | 1.82±0.02 | −0.10±0.02 | 0.369±0.002 | 1.146/615 |
|              | 1.55±0.06 | 0.16±0.06 | 0.318±0.010 | 1.111/614 |
| B3 2247+381  | 2.03±0.02 | 0.52±0.04 | 0.375±0.004 | 1.036/282 |
|              | 2.15±0.02 | 0.36±0.04 | 0.396±0.004 | 1.021/282 |
|              | 2.35±0.02 | 0.13±0.04 | 0.433±0.004 | 1.023/282 |
|              | 2.24±0.10 | 0.27±0.12 | 0.411±0.019 | 1.022/281 |
| 1ES 2344+514 | 1.86±0.01 | 0.29±0.01 | 0.528±0.003 | 1.080/531 |
|              | 1.96±0.01 | 0.18±0.02 | 0.552±0.003 | 1.093/531 |
|              | 2.40±0.01 | −0.26±0.02 | 0.685±0.004 | 1.308/531 |
|              | 1.81±0.05 | 0.33±0.06 | 0.514±0.013 | 1.080/530 |
Table 4. Fit parameters for the power-law fits. (1) The object name, (2) source of \( N_H \) value, (3)-(4) the spectral index and the normalization for the power-law fit defined in Sect. 3, (5) the reduced \( \chi^2 \) value and the number of degrees of freedom, (6) the test statistics value for F-test, (7) probability, (8) preferred spectral model: PO - for the power-law and LP - for the log-parabola model. The table is available in the online material only.

| Object     | \( N_H \) | \( \Gamma \) | \( N_p \) \( 10^{-2} \text{ cm}^{-2} \text{s}^{-1} \text{keV}^{-1} \) | \( \chi^2_{\text{red}}/\text{n.d.o.f} \) | \( F \) | p-value | Model |
|------------|-----------|-------------|---------------------------------|------------------|------|--------|-------|
| 1ES 0033+595 | LAB 1.62±0.01 | 2.581±0.037 | 1.800/367 | 264 | 1·10^{-16} | LP |
| DL 1.64±0.01 | 2.635±0.038 | 1.736/367 | 244 | 1·10^{-16} | LP |
| Will 1.84±0.02 | 3.476±0.052 | 1.143/367 | 53 | 1·10^{-12} | LP |
| free 1.99±0.03 | 4.322±0.151 | 1.013/366 | 7 | 0.02 | PO |
| RGB J0136+391 | LAB 2.17±0.01 | 0.671±0.006 | 1.321/260 | 114 | 1·10^{-16} | LP |
| DL 2.17±0.01 | 0.670±0.006 | 1.329/260 | 115 | 1·10^{-16} | LP |
| Will 2.23±0.01 | 0.711±0.007 | 1.094/260 | 57 | 1·10^{-13} | LP |
| free 2.42±0.03 | 0.830±0.018 | 0.845/259 | 7 | 0.4 | PO |

Table 5. Fit parameters for the broken power-law fits. (1) The object name, (2) source of \( N_H \) value, (3)-(6) the spectral indices, normalization and the break energy for the broken power-law fit defined in Sect. 3, (7) the reduced \( \chi^2 \) value and the number of degrees of freedom. The table is available in the online material only.

| Object     | \( N_H \) | \( \Gamma_1 \) | \( \Gamma_2 \) | \( N_b \) \( 10^{-2} \text{ cm}^{-2} \text{s}^{-1} \text{keV}^{-1} \) | \( E_b \) keV | \( \chi^2_{\text{red}}/\text{n.d.o.f} \) |
|------------|-----------|-------------|-------------|---------------------------------|-------------|------------------|
| 3C 66A     | LAB 2.462±0.017 | 1.746±0.170 | 0.139±0.001 | 3.383±0.328 | 0.949/260 |
| DL 2.540±0.018 | 1.794±0.140 | 0.145±0.001 | 3.064±0.261 | 0.961/260 |
| Will 2.615±0.020 | 1.936±0.104 | 0.150±0.001 | 2.568±0.213 | 0.985/260 |
| free 2.470±0.040 | 1.739±0.168 | 0.140±0.001 | 3.372±0.340 | 0.952/259 |
| S5 0716+714 | LAB 2.168±0.024 | 1.937±0.016 | 0.221±0.003 | 1.094±0.100 | 0.986/433 |
| DL 2.240±0.026 | 1.942±0.015 | 0.223±0.003 | 1.087±0.075 | 0.967/433 |
| Will 2.213±0.025 | 1.940±0.015 | 0.223±0.003 | 1.092±0.082 | 0.973/433 |
| free 2.511±0.085 | 1.965±0.017 | 0.231±0.002 | 1.046±0.042 | 0.942/432 |
Table 6. The summary of time-resolved spectral analysis. The table summarize the spectral parameters for the broken power-law fit to Swift/XRT data for the selected blazars. The time intervals are shown in Fig. 8-12 while the corresponding spectral fits are presented in Fig. 13. The following columns show: (1) the name of the object, (2) the selected interval, (3) the normalization, (4)-(5) the spectral indices, (6) the break energy (7) the value of reduced $\chi^2$ and the number of degree of freedom. The fits included in this Table are plotted in Fig. 13.

| Object          | Interval | $N_b$ 10$^{-3}$ cm$^{-2}$ s$^{-1}$ keV$^{-1}$ | $\Gamma_1$ | $\Gamma_2$ | $E_b$ keV | $\chi^2_{red}$/n.d.o.f |
|-----------------|----------|---------------------------------------------|------------|------------|-----------|-----------------------|
| 3C 66A          | A        | 1.173±0.023                                 | 2.420±0.042| 2.142±0.044| 1.37±0.21 | 0.998/219             |
| 3C 66A          | B        | 3.158±0.052                                 | 2.653±0.029| 1.4±1.8    | 5.2±1.8  | 0.883/139             |
| 3C 66A          | C        | 2.62±0.41                                   | 1.2±1.8    | 2.50±0.33  | 0.46±0.11| 0.801/136             |
| S5 0716+714     | A        | 1.767±0.072                                 | 2.911±0.071| 2.052±0.073| 1.18±0.11| 0.976/107             |
| S5 0716+714     | B        | 2.285±0.028                                 | 2.511±0.024| 2.035±0.030| 1.361±0.083| 0.925/310           |
| S5 0716+714     | C        | 2.220±0.029                                 | 2.258±0.025| 1.932±0.018| 1.153±0.079| 1.009/408           |
| S5 0716+714     | D        | 1.872±0.098                                 | 2.122±0.090| 1.976±0.037| 0.92±0.39 | 0.841/188             |
| W Comae         | A        | 0.855±0.079                                 | 2.550±0.016| 1.84±0.20  | 4.07±0.46 | 0.956/163             |
| W Comae         | B        | 0.263±0.014                                 | 2.18±0.10  | 1.738±0.067| 1.18±0.23 | 0.814/298             |
| 4C +21.35       | A        | 0.556±0.015                                 | 2.071±0.054| 1.437±0.032| 1.180±0.087| 0.835/253           |
| 4C +21.35       | B        | 0.393±0.028                                 | 1.71±0.13  | 1.366±0.038| 0.97±0.22 | 1.125/136             |
| 4C +21.35       | C        | 0.915±0.025                                 | 2.340±0.052| 1.454±0.036| 1.209±0.063| 0.877/230           |
| BL Lacertae     | A        | 3.132±0.035                                 | 2.346±0.039| 1.941±0.014| 1.237±0.062| 1.129/523            |
| BL Lacertae     | B        | 4.176±0.080                                 | 1.947±0.066| 1.703±0.012| 1.10±0.12 | 1.143/533             |
| BL Lacertae     | C        | 2.245±0.053                                 | 2.111±0.078| 1.782±0.016| 1.10±0.11 | 0.936/430             |
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Online material for: X-ray spectral studies of TeV γ-ray emitting blazars

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Figure 2. The X-ray spectral energy distributions of 29 selected blazars sorted by increasing flux density. The names of the sources are given in the upper part of each panel. Four power-law models using different values of $N_H$ are presented using different colours: red – $N_H$ taken from the LAB survey (Kalberla et al. 2005), blue – $N_H$ value taken from Dickey & Lockman (1990), magenta – $N_H$ value taken from Willingale et al. (2013) and green – free $N_H$ value. Data (grey points) presented in the figure are those fitted with the power-law model with the Galactic absorption value taken from LAB survey.
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Figure 2 – continued

log(E$^2$ dN/dE) [keV cm$^{-2}$ s$^{-1}$]
log(Energy) [keV]

log(Energy) [keV]
Figure 3. The X-ray spectra fitted with the log-parabola model with the Galactic absorption value taken from LAB survey and the ratios (data points divided by the folded model). The plots present spectra for: 1ES 0033+595, RGB J0136+391, 3C 66A, 1ES 0229+200, PKS 0447-437, 1ES 0502+675. The name of each object is also given in the upper right corner of each plot.
Figure 4. The X-ray spectra fitted with the log-parabola model with the Galactic absorption value taken from LAB survey and the ratios (data points divided by the folded model). The following plots present spectra for: PKS 0548-322, 1ES 0647+250, SS 0716+714, 1ES 0806+524, 1ES 1011+496, 1ES 1101-232. The name of each object is also given in the upper right corner of each plot.
Figure 5. The X-ray spectra fitted with the log-parabola model with the Galactic absorption value taken from LAB survey and the ratios (data points divided by the folded model). The following plots present spectra for: Mrk 180, RXJ1136.5+6737, 1ES 1218+304, W Comae, MS 1221.8+2452, 4C 21.35. The name of each object is also given in the upper right corner of each plot.
Figure 6. The X-ray spectra fitted with the log-parabola model with the Galactic absorption value taken from LAB survey and the ratios (data points divided by the folded model). The following plots present spectra for: 3C 279, PKS 1424+240, H 1426+428, PKS 1510-089, PG 1553+113, 1ES 1959+650. The name of each object is also given in the upper right corner of each plot.
Figure 7. The X-ray spectra fitted with the log-parabola model with the Galactic absorption value taken from LAB survey and the ratios (data points divided by the folded model). The following plots present spectra for: PKS 2005-489, PKS 2155-304, BL Lacertae, B3 2247+381, 1ES 2344+514. The name of each object is also given in the upper right corner of each plot.
### Table 2. The comparison of Galactic column density values. (1) The object name, (2)-(5) the $N_H$ values provided by Kalberla et al. (2005), Dickey & Lockman (1990), Willingale et al. (2013), respectively, (6)-(8) the free $N_H$ value obtained with the log-parabola, the power-law and the broken power-law model fitted.

| Object               | $N_{LAB}^{H}$ [10$^{20}$ cm$^{-2}$] | $N_{DL}^{H}$ [10$^{20}$ cm$^{-2}$] | $N_{H_{2}}^{H}$ [10$^{20}$ cm$^{-2}$] | $N_{W_{1}}^{H}$ [10$^{20}$ cm$^{-2}$] | $N_{L_P,free}^{H}$ [10$^{20}$ cm$^{-2}$] | $N_{P_L,free}^{H}$ [10$^{20}$ cm$^{-2}$] | $N_{B_P,free}^{H}$ [10$^{20}$ cm$^{-2}$] |
|----------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|
| SHBL J001355.9−185406 | 2.13                               | 0.17                               | 2.30                               |                                    |                                    |                                    |                                    |
| KUV 0033−1938        | 1.67                               | 1.77                               |                                    |                                    |                                    |                                    |                                    |
| 1ES 033+595           | 41.80                              | 14.40                              | 56.20                              | 59.36±0.42                        | 68.80±0.19                        |                                    |                                    |
| RGB J0136+391         | 6.00                               | 5.16                               | 7.30                               | 12.0±1.5                          | 11.10±0.53                        |                                    |                                    |
| RGB J0152+017         | 2.68                               | 2.39                               | 2.91                               |                                    |                                    |                                    |                                    |
| 3C 066A              | 7.37                               | 2.02                               | 9.40                               | 11.79±0.12                        | 6.31±0.42                         | 7.50±0.54                         |                                    |
| 1ES 0229+200          | 8.06                               | 9.20                               | 11.80                              | 7.86±1.98                         | 13.19±0.81                        |                                    |                                    |
| PKS 0301−243          | 1.70                               | 1.82                               | 1.79                               |                                    |                                    |                                    |                                    |
| IC 310               | 12.20                              | 13.30                              | 18.30                              |                                    |                                    |                                    |                                    |
| RBS 0413             | 8.84                               | 10.50                              | 12.90                              |                                    |                                    |                                    |                                    |
| 1ES 0347−121          | 3.09                               | 3.60                               | 3.65                               |                                    |                                    |                                    |                                    |
| 1ES 0414+009          | 8.85                               | 13.70                              |                                    |                                    |                                    |                                    |                                    |
| PKS 0447−439          | 1.18                               | 1.22                               | 3.57±0.27                         |                                    |                                    |                                    |                                    |
| 1ES 0502+065          | 9.37                               | 14.50                              | 16.7±0.46                         |                                    |                                    |                                    |                                    |
| VER J0521+211         | 28.60                              | 42.90                              |                                    |                                    |                                    |                                    |                                    |
| PKS 0548−322          | 2.58                               | 2.87                               | 4.41±0.22                         |                                    |                                    |                                    |                                    |
| RX J0648.7−1516       | 16.80                              | 25.50                              |                                    |                                    |                                    |                                    |                                    |
| 1ES 0647+250          | 11.80                              | 15.80                              | 17.8±0.35                         |                                    |                                    |                                    |                                    |
| RGB J0710+591         | 4.48                               | 5.23                               |                                    |                                    |                                    |                                    |                                    |
| S5 0716+714           | 3.22                               | 0.39                               | 1.92±0.22                         | 6.04±0.66                         |                                    |                                    |                                    |
| 1ES 0806+524          | 4.16                               | 4.89                               | 7.11±0.34                         |                                    |                                    |                                    |                                    |
| RBS 0723             | 3.39                               | 3.79                               |                                    |                                    |                                    |                                    |                                    |
| 1RXS J101015.9−311909 | 7.90                              | 10.20                              |                                    |                                    |                                    |                                    |                                    |
| S4 0954−65            | 4.80                               | 3.60                               | 6.30                               |                                    |                                    |                                    |                                    |
| 1ES 1011−496          | 0.84                               | 0.86                               | 3.04±0.22                         |                                    |                                    |                                    |                                    |
| 1ES 1101−232          | 5.51                               | 6.90                               | 6.36±0.49                         |                                    |                                    |                                    |                                    |
| Markarian 421         | 1.91                               | 2.01                               |                                    |                                    |                                    |                                    |                                    |
| Markarian 180         | 1.17                               | 1.22                               | 3.67±0.26                         |                                    |                                    |                                    |                                    |
| RX J1136.5+6737       | 1.03                               | 1.22                               | 3.57±0.47                         |                                    |                                    |                                    |                                    |
| 1ES 1215+303          | 1.70                               | 1.80                               |                                    |                                    |                                    |                                    |                                    |
| 1ES 1215+304          | 1.99                               | 2.12                               | 3.05±0.37                         |                                    |                                    |                                    |                                    |
| W Comae              | 2.04                               | 2.18                               | 8.75±0.32                         | 2.54±0.50                         |                                    |                                    |                                    |
| MS 1221.8+2452        | 1.79                               | 1.91                               | 5.73±0.43                         |                                    |                                    |                                    |                                    |
| 4C +21.35            | 2.12                               | 2.29                               | 1.07±0.73                         |                                    |                                    |                                    |                                    |
| S3 1227+25            | 2.01                               | 1.50                               |                                    |                                    |                                    |                                    |                                    |
| 3C 279               | 7.77                               | 11.20                              |                                    |                                    |                                    |                                    |                                    |
| 1ES 1312−423          | 7.93                               | 3.42                               |                                    |                                    |                                    |                                    |                                    |
| PKS 1424+240          | 2.84                               | 3.19                               | 6.25±0.32                         |                                    |                                    |                                    |                                    |
| H 1426+428            | 1.11                               | 1.14                               | 3.12±0.15                         |                                    |                                    |                                    |                                    |
| 1ES 1440+122          | 1.58                               | 1.72                               |                                    |                                    |                                    |                                    |                                    |
| PKS 1441+25           | 3.12                               | 3.49                               |                                    |                                    |                                    |                                    |                                    |
| PKS 1510−089          | 6.99                               | 9.45                               | 5.28±0.25                         |                                    |                                    |                                    |                                    |
| AP Librae            | 8.36                               | 4.17                               |                                    |                                    |                                    |                                    |                                    |
| PG 1553+113           | 3.67                               | 4.35                               | 5.03±0.20                         |                                    |                                    |                                    |                                    |
| Markarian 501         | 1.58                               | 1.66                               |                                    |                                    |                                    |                                    |                                    |
| H 1722+119            | 8.70                               | 13.80                              |                                    |                                    |                                    |                                    |                                    |
| 1ES 1727+502          | 2.38                               | 2.60                               |                                    |                                    |                                    |                                    |                                    |
| 1ES 1741+196          | 7.32                               | 9.58                               |                                    |                                    |                                    |                                    |                                    |
| HESS J1943.2−213      | 82.40                              | 96.80                              |                                    |                                    |                                    |                                    |                                    |
| 1ES 1959+650          | 9.83                               | 15.90                              | 11.1±0.31                         |                                    |                                    |                                    |                                    |
| MAGIC J2001.4+335     | 37.00                              | 51.40                              |                                    |                                    |                                    |                                    |                                    |
| PKS 205−489           | 3.94                               | 4.66                               | 3.54±0.25                         |                                    |                                    |                                    |                                    |
| PKS 2155−304          | 1.52                               | 1.63                               | 3.51±0.43                         |                                    |                                    |                                    |                                    |
| BL Lacertae          | 18.30                              | 27.59                              | 25.09±1.02                        |                                    |                                    |                                    |                                    |
| BL Lacertae+381       | 10.20                              | 15.40                              |                                    |                                    |                                    |                                    |                                    |
| RGB J2243+203         | 5.25                               | 6.33                               |                                    |                                    |                                    |                                    |                                    |
| 1ES 2344+514          | 15.10                              | 19.18                              |                                    |                                    |                                    |                                    |                                    |
| H 2356−309            | 1.42                               | 1.48                               |                                    |                                    |                                    |                                    |                                    |
Table 4. Fit parameters for the power-law fits. (1) The object name, (2) source of $N_H$ value, (3)-(4) the spectral index and the normalization for the power-law fit defined in Sect. 3, (5) the reduced $\chi^2$ value and the number of degrees of freedom, (6) the test statistics value for F-test, (7) probability, (8) preferred spectral model: PO - for the power-law and LP - for the log-parabola model.

| Object          | $N_H$   | $\Gamma$ | $N_p$ | $\chi^2$/nd.o.f | $F$ | p-value | Model |
|-----------------|---------|----------|-------|-----------------|-----|---------|-------|
|                 | (1)     | (2)      | (3)   | (4)             | (5) | (6)     | (7)   |
| 1ES0033+595     | LAB     | 1.62±0.01| 2.581±0.037| 1.800±0.367| 264 | 1.10^{-16} | LP    |
|                 | DL      | 1.64±0.01| 2.635±0.038| 1.736±0.367| 244 | 1.10^{-16} | LP    |
|                 | Will    | 1.84±0.02| 3.476±0.052| 1.143±0.367| 53  | 1.10^{-12} | LP    |
|                 | free    | 1.99±0.03| 4.322±0.151| 1.013±0.366| 5   | 0.02    | PO    |
|                 | RGB     | 2.17±0.01| 0.671±0.006| 1.321±0.260| 114 | 1.10^{-16} | LP    |
| J0136+391       | LAB     | 2.17±0.01| 0.670±0.006| 1.329±0.260| 115 | 1.10^{-16} | LP    |
|                 | DL      | 2.17±0.01| 0.711±0.007| 1.094±0.260| 57  | 1.10^{-13} | LP    |
|                 | Will    | 2.23±0.01| 0.830±0.018| 0.845±0.259| 0.7 | 0.4     | PO    |
|                 | free    | 2.42±0.03| 0.140±0.001| 1.066±0.262| 21  | 6.10^{-6} | LP    |
|                 | 3C66A   | 1.59±0.02| 0.370±0.005| 1.381±0.266| 51  | 8.10^{-12} | LP    |
|                 | LAB     | 1.62±0.02| 0.385±0.005| 1.300±0.266| 32  | 4.10^{-8} | LP    |
|                 | DL      | 1.70±0.02| 0.421±0.006| 1.202±0.266| 6   | 0.01    | PO    |
|                 | Will    | 1.74±0.03| 0.441±0.013| 1.194±0.265| 7   | 7.10^{-3} | LP    |
|                 | free    | 2.51±0.01| 0.623±0.004| 1.474±0.274| 70  | 3.10^{-15} | LP    |
|                 | PKS     | 1.26±0.01| 1.227±0.009| 1.885±0.349| 247 | 1.10^{-16} | LP    |
|                 | 0447−439| LAB     | 1.26±0.01| 1.237±0.009| 1.833±0.349| 228 | 1.10^{-16} | LP    |
|                 | DL      | 2.26±0.01| 1.497±0.011| 1.079±0.349| 17  | 5.10^{-5} | LP    |
|                 | Will    | 2.33±0.02| 1.597±0.028| 1.031±0.348| 1   | 0.6     | PO    |
|                 | free    | 1.80±0.01| 1.001±0.005| 1.142±0.530| 104 | 1.10^{-16} | LP    |
|                 | PKS     | 1.78±0.01| 0.984±0.005| 1.216±0.530| 146 | 1.10^{-16} | LP    |
|                 | 0548−322| LAB     | 1.81±0.01| 1.014±0.005| 1.098±0.530| 78  | 1.10^{-16} | LP    |
|                 | DL      | 1.87±0.01| 1.080±0.011| 1.000±0.529| 25  | 9.10^{-7} | LP    |
|                 | Will    | 2.16±0.01| 0.915±0.005| 2.013±0.427| 328 | 1.10^{-16} | LP    |
|                 | free    | 2.32±0.01| 1.062±0.006| 1.206±0.427| 42  | 3.10^{-10} | LP    |
|                 | S50716+714| LAB   | 2.39±0.02| 1.138±0.015| 1.155±0.426| 12  | 5.10^{-4} | LP    |
|                 | DL      | 2.06±0.01| 0.232±0.001| 1.145±0.435| 50  | 6.10^{-12} | LP    |
|                 | Will    | 2.05±0.01| 0.235±0.001| 1.195±0.435| 73  | 2.10^{-16} | LP    |
|                 | free    | 1.96±0.01| 0.219±0.002| 1.069±0.434| 19  | 1.10^{-5} | LP    |
|                 | 1ES     | 2.42±0.01| 0.393±0.003| 1.316±0.285| 93  | 1.10^{-16} | LP    |
|                 | 0647+250| LAB     | 2.44±0.01| 0.398±0.003| 1.252±0.285| 76  | 2.10^{-16} | LP    |
|                 | DL      | 2.46±0.01| 0.406±0.003| 1.171±0.285| 55  | 2.10^{-12} | LP    |
|                 | Will    | 2.59±0.02| 0.446±0.007| 1.003±0.284| 6   | 0.02    | LP    |
|                 | free    | 2.29±0.01| 0.895±0.005| 1.606±0.361| 97  | 1.10^{-16} | LP    |
|                 | 1ES     | 2.29±0.01| 0.892±0.005| 1.622±0.361| 101 | 1.10^{-16} | LP    |
|                 | 1011+496| LAB     | 2.29±0.01| 0.895±0.005| 1.600±0.361| 96  | 1.10^{-16} | LP    |
|                 | DL      | 2.11±0.02| 0.986±0.020| 1.049±0.270| -0.1| 1       | PO    |
|                 | Will    | 2.09±0.03| 1.945±0.042| 1.049±0.269| 6   | 0.01    | PO    |
|                 | free    | 2.09±0.03| 1.945±0.042| 1.049±0.269| 6   | 0.01    | PO    |
Table 4 – continued

|     | (1)  | (2)   | (3)    | (4)   | (5)   | (6)   | (7)   | (8)   |
|-----|------|-------|--------|-------|-------|-------|-------|-------|
| Mrk 180 | LAB | 2.15±0.01 | 0.808±0.005 | 1.326/240 | -24 | 1 | PO |
|  | DL | 2.16±0.01 | 0.818±0.005 | 1.259/340 | 87 | 10^{-16} | LP |
|  | Will | 2.15±0.01 | 0.810±0.005 | 1.312/340 | 102 | 10^{-16} | LP |
|  | free | 2.28±0.02 | 0.905±0.011 | 0.999/339 | 3 | 0.07 | PO |
| RX J1136.5+6737 | LAB | 1.73±0.01 | 0.401±0.004 | 1.171/272 | 35 | 10^{-8} | LP |
|  | DL | 1.75±0.01 | 0.407±0.004 | 1.141/272 | 27 | 3.10^{-7} | LP |
|  | Will | 1.73±0.01 | 0.402±0.004 | 1.168/272 | 34 | 10^{-8} | LP |
|  | free | 1.84±0.03 | 0.448±0.010 | 1.650/271 | 3 | 0.1 | PO |
| 1ES 1218+304 | LAB | 2.07±0.01 | 0.906±0.008 | 1.248/288 | 13 | 4.10^{-4} | LP |
|  | DL | 2.06±0.01 | 0.896±0.008 | 1.264/288 | 18 | 4.10^{-5} | LP |
|  | Will | 2.08±0.01 | 0.911±0.008 | 1.240/288 | 11 | 10^{-3} | LP |
|  | free | 2.12±0.02 | 0.948±0.017 | 1.220/287 | 7 | 0.01 | LP |
| W Comae | LAB | 2.42±0.01 | 0.068±0.001 | 1.160/254 | 37 | 4.10^{-9} | LP |
|  | DL | 2.41±0.01 | 0.067±0.001 | 1.144/254 | 26 | 7.10^{-7} | LP |
|  | Will | 2.43±0.01 | 0.068±0.001 | 1.172/254 | 42 | 5.10^{-10} | LP |
|  | free | 2.34±0.03 | 0.065±0.001 | 1.113/253 | 39 | 2.10^{-9} | LP |
| MS 1221.8+2452 | LAB | 2.25±0.01 | 0.366±0.005 | 1.563/241 | 90 | 10^{-16} | LP |
|  | DL | 2.25±0.01 | 0.367±0.003 | 1.561/241 | 89 | 10^{-16} | LP |
|  | Will | 2.25±0.01 | 0.368±0.003 | 1.533/241 | 84 | 10^{-16} | LP |
|  | free | 2.47±0.03 | 0.438±0.009 | 1.112/240 | 1 | 0.2 | PO |
| 4C +21.35 | LAB | 1.69±0.01 | 0.068±0.001 | 1.763/375 | 267 | 10^{-16} | LP |
|  | DL | 1.69±0.01 | 0.068±0.001 | 1.795/375 | 276 | 10^{-16} | LP |
|  | Will | 1.70±0.01 | 0.068±0.001 | 1.802/375 | 278 | 10^{-16} | LP |
|  | free | 1.60±0.02 | 0.063±0.001 | 1.349/374 | 123 | 10^{-16} | LP |
| 3C 279 | LAB | 1.54±0.01 | 0.240±0.001 | 1.293/608 | 102 | 10^{-16} | LP |
|  | DL | 1.55±0.01 | 0.242±0.001 | 1.260/608 | 83 | 10^{-16} | LP |
|  | Will | 1.55±0.01 | 0.242±0.001 | 1.259/608 | 84 | 10^{-16} | LP |
|  | free | 1.61±0.01 | 0.257±0.002 | 1.152/607 | 25 | 7.10^{-7} | LP |
| H 1426+428 | LAB | 1.90±0.01 | 1.373±0.005 | 1.678/584 | 204 | 10^{-16} | LP |
|  | DL | 1.91±0.01 | 1.390±0.005 | 1.583/584 | 159 | 10^{-16} | LP |
|  | Will | 1.90±0.01 | 1.374±0.005 | 1.667/584 | 199 | 10^{-16} | LP |
|  | free | 1.99±0.01 | 1.498±0.011 | 1.317/583 | 34 | 10^{-8} | LP |
| PKS 1424+240 | LAB | 2.52±0.01 | 0.245±0.002 | 1.498/268 | 104 | 10^{-16} | LP |
|  | DL | 2.50±0.01 | 0.243±0.002 | 1.560/268 | 116 | 10^{-16} | LP |
|  | Will | 2.54±0.01 | 0.250±0.002 | 1.384/268 | 83 | 10^{-16} | LP |
|  | free | 2.73±0.02 | 0.285±0.004 | 0.966/267 | 0.4 | 0.5 | PO |
| PKS 1510−089 | LAB | 1.34±0.01 | 0.107±0.001 | 1.096/661 | 33 | 10^{-8} | LP |
|  | DL | 1.36±0.01 | 0.110±0.001 | 1.168/661 | 68 | 10^{-15} | LP |
|  | Will | 1.40±0.01 | 0.116±0.001 | 1.379/661 | 166 | 10^{-16} | LP |
|  | free | 1.29±0.01 | 0.102±0.001 | 1.632/660 | 0.4 | 0.5 | PO |
| PG 1553+113 | LAB | 2.28±0.01 | 1.023±0.004 | 1.405/433 | 36 | 40.10^{-9} | LP |
|  | DL | 2.28±0.01 | 1.023±0.004 | 1.402/433 | 36 | 5.10^{-9} | LP |
|  | Will | 2.32±0.01 | 1.053±0.005 | 1.314/433 | 10 | 2.10^{-3} | LP |
|  | free | 2.35±0.01 | 1.084±0.010 | 1.288/432 | 0.3 | 0.6 | PO |
| 1ES 1959+650 | LAB | 2.06±0.01 | 6.050±0.036 | 2.116/467 | 316 | 10^{-16} | LP |
|  | DL | 2.08±0.01 | 7.082±0.037 | 1.967/467 | 281 | 10^{-16} | LP |
|  | Will | 2.29±0.01 | 8.676±0.046 | 1.329/467 | 0.3 | 0.6 | PO |
|  | free | 2.26±0.01 | 8.448±0.100 | 1.317/466 | 22 | 3.10^{-6} | LP |

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Table 4 – continued

| (1)      | (2)      | (3)      | (4)      | (5)      | (6)      | (7)      | (8)      |
|----------|----------|----------|----------|----------|----------|----------|----------|
| PKS 2005−489 LAB | 2.47±0.01 | 0.927±0.006 | 0.990/327 | 3 0.1 | PO |
| DL       | 2.53±0.01 | 0.970±0.006 | 1.083/327 | 30 1·10−7 | LP |
| Will     | 2.51±0.01 | 0.955±0.006 | 1.040/327 | 18 3·10−5 | LP |
| free     | 2.44±0.02 | 0.911±0.011 | 0.986/326 | 0.7 0.4 | PO |
| PKS 2155−304 LAB | 2.40±0.02 | 3.671±0.037 | 1.261/209 | 21 9·10−6 | LP |
| DL       | 2.41±0.02 | 3.704±0.037 | 1.239/209 | 17 4·10−5 | LP |
| Will     | 2.41±0.02 | 3.690±0.037 | 1.248/209 | 19 2·10−5 | LP |
| free     | 2.53±0.03 | 4.013±0.085 | 1.153/208 | 1 0.2 | PO |
| BL Lacertae LAB | 1.50±0.01 | 0.267±0.002 | 2.002/616 | 444 1·10−16 | LP |
| DL       | 1.58±0.01 | 0.294±0.002 | 1.452/616 | 182 1·10−16 | LP |
| Will     | 1.76±0.01 | 0.366±0.002 | 1.172/616 | 15 1·10−4 | LP |
| free     | 1.71±0.01 | 0.344±0.004 | 1.121/615 | 6 0.01 | PO |
| BL Lacertae LAB | 1.50±0.01 | 0.267±0.002 | 2.002/616 | 444 1·10−16 | LP |
| DL       | 1.58±0.01 | 0.294±0.002 | 1.452/616 | 182 1·10−16 | LP |
| Will     | 1.76±0.01 | 0.366±0.002 | 1.172/616 | 15 1·10−4 | LP |
| free     | 1.71±0.01 | 0.344±0.004 | 1.121/615 | 6 0.01 | PO |
| BL Lacertae LAB | 1.50±0.01 | 0.267±0.002 | 2.002/616 | 444 1·10−16 | LP |
| DL       | 1.58±0.01 | 0.294±0.002 | 1.452/616 | 182 1·10−16 | LP |
| Will     | 1.76±0.01 | 0.366±0.002 | 1.172/616 | 15 1·10−4 | LP |
| free     | 1.71±0.01 | 0.344±0.004 | 1.121/615 | 6 0.01 | PO |
| BL Lacertae LAB | 1.50±0.01 | 0.267±0.002 | 2.002/616 | 444 1·10−16 | LP |
| DL       | 1.58±0.01 | 0.294±0.002 | 1.452/616 | 182 1·10−16 | LP |
| Will     | 1.76±0.01 | 0.366±0.002 | 1.172/616 | 15 1·10−4 | LP |
| free     | 1.71±0.01 | 0.344±0.004 | 1.121/615 | 6 0.01 | PO |
| BL Lacertae LAB | 1.50±0.01 | 0.267±0.002 | 2.002/616 | 444 1·10−16 | LP |
| DL       | 1.58±0.01 | 0.294±0.002 | 1.452/616 | 182 1·10−16 | LP |
| Will     | 1.76±0.01 | 0.366±0.002 | 1.172/616 | 15 1·10−4 | LP |
| free     | 1.71±0.01 | 0.344±0.004 | 1.121/615 | 6 0.01 | PO |
| BL Lacertae LAB | 1.50±0.01 | 0.267±0.002 | 2.002/616 | 444 1·10−16 | LP |
| DL       | 1.58±0.01 | 0.294±0.002 | 1.452/616 | 182 1·10−16 | LP |
| Will     | 1.76±0.01 | 0.366±0.002 | 1.172/616 | 15 1·10−4 | LP |
| free     | 1.71±0.01 | 0.344±0.004 | 1.121/615 | 6 0.01 | PO |

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Table 5. Fit parameters for the broken power-law fits. (1) The object name, (2) source of $N_H$ value, (3)-(6) the spectral indices, normalization and break energy for the broken power-law fit defined in Sect. 3, (7) the reduced $\chi^2$ value and the number of degrees of freedom.

| Object          | $N_H$   | $\Gamma_1$ | $\Gamma_2$ | $N_b$ | $E_b$ (keV) | $\chi^2_{\text{red}}$/n.d.o.f |
|-----------------|---------|------------|------------|-------|-------------|-----------------------------|
| 3C 66A LAB      | 2.462±0.017 | 1.746±0.170 | 0.139±0.001 | 3.383±0.328 | 0.949/260     |
| DL              | 2.540±0.018 | 1.794±0.140 | 0.145±0.001 | 3.064±0.261 | 0.961/260     |
| Will            | 2.615±0.020 | 1.936±0.104 | 0.150±0.001 | 2.568±0.213 | 0.985/260     |
| free            | 2.470±0.040 | 1.739±0.168 | 0.140±0.001 | 3.372±0.340 | 0.952/259     |
| S5 0716+714 LAB | 2.168±0.024 | 1.937±0.016 | 0.221±0.003 | 1.094±0.100 | 0.986/433     |
| DL              | 2.240±0.026 | 1.942±0.015 | 0.223±0.003 | 1.087±0.075 | 0.967/433     |
| Will            | 2.213±0.025 | 1.940±0.015 | 0.223±0.003 | 1.092±0.082 | 0.973/433     |
| free            | 2.511±0.085 | 1.965±0.017 | 0.231±0.002 | 1.046±0.042 | 0.942/432     |
| W Comae LAB     | 2.492±0.019 | 2.076±0.074 | 0.066±0.001 | 2.027±0.234 | 0.988/252     |
| DL              | 2.474±0.018 | 2.080±0.076 | 0.066±0.001 | 2.047±0.252 | 0.993/252     |
| Will            | 2.504±0.019 | 2.070±0.071 | 0.669±0.001 | 2.028±0.218 | 0.986/252     |
| free            | 2.538±0.050 | 2.071±0.069 | 0.677±0.001 | 1.976±0.212 | 0.987/251     |
| 4C+21.35 LAB    | 2.106±0.034 | 1.442±0.021 | 0.061±0.001 | 1.183±0.054 | 0.989/373     |
| DL              | 2.124±0.034 | 1.444±0.021 | 0.062±0.001 | 1.177±0.052 | 0.990/373     |
| Will            | 2.128±0.034 | 1.444±0.021 | 0.616±0.001 | 1.176±0.052 | 0.991/373     |
| free            | 1.978±0.093 | 1.432±0.022 | 0.604±0.001 | 1.222±0.071 | 0.987/372     |
| BL Lacertae LAB| 1.155±0.023 | 1.705±0.014 | 0.260±0.002 | 1.611±0.048 | 1.173/614     |
| DL              | 1.374±0.021 | 1.728±0.016 | 0.286±0.002 | 1.766±0.081 | 1.122/614     |
| Will            | 1.996±0.047 | 1.727±0.010 | 0.363±0.005 | 1.095±0.087 | 1.098/614     |
| free            | 1.570±0.056 | 1.740±0.019 | 0.318±0.010 | 1.983±0.232 | 1.105/613     |
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