In this study, we examined various forms of mathematical models that are relevant for the containment, risk analysis, and features of COVID-19. Greater emphasis was laid on the extension of the Susceptible–Infectious–Recovered (SIR) models for policy relevance in the time of COVID-19. These mathematical models play a significant role in the understanding of COVID-19 transmission mechanisms, structures, and features. Considering that the disease has spread sporadically around the world, causing large scale socioeconomic disruption unwitnessed in contemporary ages since World War II, researchers, stakeholders, government, and the society at large are actively engaged in finding ways to reduce the rate of infection until a cure or vaccination procedure is established. We advanced argument for the various forms of the mathematical model of epidemics and highlighted their relevance in the containment of COVID-19 at the present time. Mathematical models address the need for understanding the transmission dynamics and other significant factors of the disease that would aid policymakers to make accurate decisions and reduce the rate of transmission of the disease.

1 INTRODUCTION

Severe Acute Respiratory Syndrome Coronavirus-2 (SARS-CoV-2), a novel β-coronavirus is the pathogen responsible for the coronavirus disease 2019 (COVID-19; Li, Geng, Peng, Meng, & Lu, 2020). The novel coronavirus has spread across the globe with the attendant consequences felt in about 203 countries. As at the time of writing (June 18, 2020), there are about 8,061,550 confirmed COVID-19 cases with 440,290 attributable deaths (World Health Organization [WHO], 2020). The Americas (North and South) account for close to 50% of global cases with values standing at 3,899,859 confirmed cases and 205,555 deaths. In Europe, there are about 2,452,247 confirmed cases with about 189,582 attributable deaths. In the Eastern Mediterranean region, cases have soared to 817,458 with fatalities around 18,057. In the Southeastern Asia region, about 503,034 cases have been recorded with around 15,498 deaths. Down in the western Pacific, there are about 200,586 cases with about 7,239 attributable deaths. Across the African region, the number of confirmed cases stood at 187,625 with 4,346 deaths (WHO, 2020). Since the emergence of the virus in Wuhan, China in December 2019, the aerosolized pathogens have spread exponentially, causing a large scale and unprecedented socio and economic disruptions, threat to global public health systems, poverty, undesirable psychological depression, more considerable uncertainties among many other deep-rooted issues (Sameni, 2020). The viral genome sequence of the SARS-CoV-2 suggests the close relatedness to SARS-like bat CoVs, but most genomic encoded proteins of the SARS-CoV-2 are similar to the SARS-CoVs with differences in two of the non-structural proteins (NSP2 and NSP3), spike protein and the receptor-binding domain (RBD; Wu et al., 2020). Studies have shown that the SARS-CoV-2 is capable of mutation with two types being majorly classified as the L-type and the S-type (Tang et al., 2020). The S-type has been reported to have evolved when jumping from animal to man while the L-type evolved later. Although both are currently involved in the pandemic, the L-type has been reported to be more prevalent than the S-type (Guo et al., 2020). How mathematical models explain these chain reactions and transmission mechanisms forms the core of the foregoing.
Severity, features, structures risk analysis, and containment of the virus have been studied along with various disciplines and dimensions (Adekunle, Onanuga, Akinola & Ogubanjo, 2020). A notable consensus has been the adoption of social distancing and practice of good hygiene as a measure to deter virus proliferation and flatten the epidemic growth curve such that fast-rising number of COVID-19 attributable deaths can be reduced (Sameni, 2020). However, empirical ambiguity still persists on the mechanical (mathematical) nature of the transmission pattern. Mathematical models are well-positioned to explain the evolutionary nature of epidemic outbreaks and the spread pattern. A review of the mathematical models with attendant structural evolution for the transmission dynamics of COVID-19 could be an essential finding in the containment, risk analysis, and search for the cure of the disease.

With the global pandemic leading to the increase in morbidity and mortality of the global population, socioeconomic, and public health disarray (Van Zandvoort et al., 2020), the agonizing consequences of the novel coronavirus on public health are influencing new waves of research on the relevance of mathematical models in predicting the sequence of the virus and its propagation pattern. With the proper understanding of the evolutionary and dynamic growth pattern of COVID-19 using mathematical models, public health officials, government, and the society at large can take a giant step forward in their fight against COVID-19 amidst global uncertainties (Nandal, 2020). Several researchers in the scientific community have carried out interdisciplinary studies to understand the virus propagation pattern using various mathematical models (see Ivorra, Ferrández, Vela-Pérez, & Ramos, 2020; Kim, Seo, & Jung, 2020; Ndaïrou, Area, Nieto, & Torres, 2020; Torrealba-Rodríguez, Conde-Gutiérrez, & Hernández-Javier, 2020 for some examples). However, a holistic approach of mathematical instrumentalization models in the analysis of COVID-19 growth curve and its containment strategies remains grossly understudied in extant literature. The intricacies of this unobserved factor underpin this study. We complement available studies on the subject matter and extend the SIR models and rely on inferences drawn from available studies using the extensions of SIR models. The application of these models consists of the use of mathematical tools and a specific language to explain and predict the behavior of the infectious viral disease. These models could be deterministic, non-deterministic, or could contain branching processes that aid the prediction of the infectious disease.

2 | MATHEMATICAL MODELS

Mathematical models help to make mental models quantitative; it involves writing down a set of equations that mimics reality which is then solved for specific values of the parameters within the equations (Panovska-Griffiths, 2020; Revathi & Rangnathan, 2020). Mathematical modeling simplifies reality and answers questions using subsets of data (Panovska-Griffiths, 2020). Predictive mathematical models are essential for understanding the course of an epidemic. One of the most commonly used models is the Susceptible–Infectious–Recovered (SIR) models for the human to human transmission (Giordano et al., 2020). However, modelers need to acquire at least one dataset with relevant data points before developing or validating a model (Nandal, 2020). Predictive models for large countries could be problematic because they aggregate heterogeneous sub-epidemics (Jewell, Lewnard, & Jewell, 2020). Various factors, such as individual characteristics and population distribution, have a significant contribution, thus affecting the model prediction (Jewell et al., 2020).

2.1 | Models for airborne viral diseases

2.1.1 | Susceptible–infectious–recovered

The underlying mathematical model which has been developed as far back in the 1920s is still in use today, and this basic model is referred to as the SIR model (Freiberger, 2014). The SIR model divided the population into three groups as in Shil (2016); the susceptible (S), the infectious (I), and the recovered (R). It was developed by Kernack and McKendrick to describe an influenza epidemic (Bauer, 2017). It assumes the introduction of an infected individual into a population where the members have not been previously exposed to the pathogen. Therefore, all are susceptible (S), each infected individual (I) transmits to susceptible members of the population with a mean transmission rate \( \beta \). At the end of the infectious period, individuals who recover from the infections are referred to as the recovered (R) member of the population, if the mean recovery rate is \( \alpha \), then the mean transmission period in any individual is given by \( 1/\alpha \). The differential equations describing the transmission as per the basic SIR model is given by

\[
\frac{dS(t)}{dt} = -\beta S(t)I(t) \\
\frac{dI(t)}{dt} = \beta S(t)I(t) - \alpha I(t) \\
\frac{dR(t)}{dt} = \alpha I(t)
\]

where \( S(t) \) and \( I(t) \) represents the number of individuals in the susceptible and infectious states respectively at any time \( t \), while the rates of change of \( S(t) \) and \( I(t) \) with time is represented by \( dS(t) \) and \( dI(t) \), respectively.

If the population is considered constant with no agent leaving or coming into the system, the equation is given by:

\[
N = S(t) + I(t) + R(t)
\]

The number of susceptible individuals decreases as the number of incidences increases, so also the epidemic declines, as more individuals recover from the disease (Shil, 2016). Basic reproduction number is a phenomenon where the average number of secondary infections
generated by one infectious individual when introduced into a fully susceptible population is measured, $R_0$ denotes it. The severity of an epidemic and rate of progression depends on the value of the basic reproduction number, so if $R_0$ is greater than 1, the epidemic will continue, but if it is less than 1 then the epidemic would fade out (Delameter, Street, Leslie, Yang, & Jacobsen, 2019). The basic reproduction number can be calculated from the growth rate ($\lambda$) of the epidemic obtained from the cumulative incidences data in the initial growth phase of the outbreak as

$$R_0 = \left(1 + \frac{\lambda}{\infty}\right)$$

(5)

The numerical solutions of the ordinary differential equations can be obtained with an appropriate application using computer simulations, and this model has been used to explain the transmission and repeated outbreaks of measles in New York between 1930 and 1962. The SIR model can be further modified considering demographics and weather/seasonal variations. Modified SIR has been used to explain viral epidemics such as Influenza justifying its applicability to the COVID-19 context.

### 2.1.2 Susceptible–exposed–infectious–recovered

Certain infectious diseases have an incubation period or exposed stage in an individual following infection until the symptoms are observed. In other words, the susceptible–exposed–infectious–recovered (SEIR) account for the exposed or latent stage (Shil, 2016). Here each individual who receives the virus exists in the exposed or latent state ($E$) during which the virus is incubated but does not transmit the infection to anyone, so with the onset of symptoms the individual makes a transition to the infectious state. Considering the constant population size

$$N = S + E + I + R$$

(6)

and the set of differential equations as:

Recall Equation (1) $\frac{dS(t)}{dt} = -\beta S(t)I(t)$ and Equation (2) $\frac{dI(t)}{dt} = \beta S(t)I(t) - \alpha I(t)$ to generate

$$\frac{dE(t)}{dt} = \beta S(t)I(t) - \alpha E(t)$$

(7)

While Equation (3) remains as $\frac{dR(t)}{dt} = \alpha L(t)$.

The basic reproduction of the SEIR model can be determined using the formula

$$R_0 = \left(1 + \frac{R}{\infty}\right) \left(1 + \frac{R}{\infty}\right)$$

(8)

where the mean infective period is $1/\alpha$ while the mean incubation period is $1/k$.

The SEIR model with suitable adaptations has been widely applied for various disease epidemics such as chickenpox and SARS, and its relevance has been advanced for the analysis of the dynamic transmission of COVID-19 in this context.

### 2.1.3 Susceptible–exposed–infectious–asymptomatic–recovered

This is a simple model for viral epidemics involving asymptomatic individuals in the population in a situation without any interventions. Individuals testing positive in serological tests or blood tests for disease without symptoms is referred to as asymptomatic and is denoted as A in the susceptible–exposed–infectious–asymptomatic–recovered (SEIAR) model, so considering a constant population;

$$N = S(t) + E(t) + I(t) + A(t) + R(t)$$

(9)

This indicates the total population was susceptible, and there was no transmission from individuals at the latent state and a fraction of the proceeds to the infectious state. In contrast, other fractions ($I - p$) proceed to the asymptomatic state at the same time ($k$) with the asymptomatic individuals having a reduced ability to transmit the infection. If $q$ is the factor that determines transmissibility in asymptomatic individuals, then $0 < q < 1$. The ordinary differential equation of the transmission process can be described as the following.

$$\frac{dS}{dt} = -\beta S(t)(1 + qA)$$

(10)

$$\frac{dE}{dt} = \beta S(t)(1 + qA) - kE$$

(11)

$$\frac{dl}{dt} = pE - \alpha l$$

(12)

$$\frac{dA}{dt} = (1 - p)kE - \Pi A$$

(13)

$$\frac{dR}{dt} = \alpha l + \Pi A$$

(14)

$$\frac{dC}{dt} = \alpha l$$

(15)

where $C$ denotes the cumulative number of infectives. This model was used to explain the transmission dynamics of the swine flu outbreak in 2009 at a residential school in Maharashtra, India (Shil, 2016).

### 2.1.4 Complex SEIAR (hospitalization)

This model describes the incorporation of the hospitalization of a fraction of infectious individuals. Here the population is classified into
SEIAR with $J(t)$ and $D(t)$ denoting the hospitalized and dead respectively. Considering the total population is constant at any time,

$$N = S(t) + E(t) + I(t) + A(t) + J(t) + D(t)$$  \hspace{1cm} (16)

The ordinary differential equation of the transmission process is described as the following

$$\frac{dS}{dt} = \mu N(t) - \beta S(t) I(t) - J(t) - qA(t) - \mu S(t)$$  \hspace{1cm} (17)

$$\frac{dE}{dt} = \beta S(t) I(t) + J(t) + qA(t) - (k + \mu)E(t)$$  \hspace{1cm} (18)

$$\frac{dA}{dt} = k(1-p)E(t) - (\gamma 1 + \mu)A(t)$$  \hspace{1cm} (19)

$$\frac{dJ}{dt} = kpE(t) - (\alpha + \gamma 1 + \mu)J(t)$$  \hspace{1cm} (20)

$$\frac{dI}{dt} = aI(t) - (\delta + \gamma 2 + \mu)J(t)$$  \hspace{1cm} (21)

$$\frac{dR}{dt} = \gamma 1 (A(t) + I(t)) + \gamma 2 J(t) - \mu R(t)$$  \hspace{1cm} (22)

$$\frac{dD}{dt} = \delta I(t)$$  \hspace{1cm} (23)

$$\frac{dC}{dt} = aI(t)$$  \hspace{1cm} (24)

The $\mu$ represents the rate of birth and natural death, while the cumulative number of infections is represented by $C(t)$. Epidemic data of the Spanish Flu pandemic in Geneva was obtained using the Complex SEIAR model, and all parameters of the model were determined.

The SEIR and SEIAR models have been further extended by involving various parameters to play crucial roles in public health interventions, quarantine, travel restrictions, vaccination, or dosage of antivirals (Shil, 2016).

### 3 | MODELLING THE COVID-19 PANDEMIC

Globally, radical alteration with rapidly changing socioeconomic dynamics has been occurring due to the COVID-19 Pandemic. Several countries have been on full or partial lockdown while adhering to social distancing measures as they wait for a specific treatment modality such as vaccines (Sinha, 2020). Public information such as incidence or prevalence of infection, morbidity, or mortality due to COVID-19 could be used to solve mathematical models, solutions from these models are then recalibrated repetitively until it is suitable for prediction of the future behavior of SARS-CoV-2 (Panovska-Griffiths, 2020).

The COVID-19 Pandemic has been modeled by various researchers with the aim of stimulating the infections within the population (Shaikh, Shaikh, & Nisar, 2020). Most models represent individual to transition between compartments in a given community, these compartments are based on each individual's infectious state, and related population sizes with respect to time (Shaikh et al., 2020). Lin et al. (2020) had suggested a conceptual model for COVID-19, this model effectively catches the timeline of the disease epidemic while Chen et al. (2020) examined a model based on stage based transmissibility of the SARS-CoV-2 (Chen et al., 2020; Lin et al., 2020). Whereas Khan and Atangana (2020) formulated a model of people versus COVID-19, the model is given as

$$\frac{dS}{dt} = \Delta - \lambda S - \frac{aS(t) + \beta A(t)}{N} - \gamma SQ,$$  \hspace{1cm} (25)

$$\frac{dE}{dt} = S(t) + \beta S(t) I(t) - (1 - \phi) \delta E - \phi \mu E - \lambda E,$$  \hspace{1cm} (26)

$$\frac{dA}{dt} = (1 - \phi) \delta E - (\sigma + \lambda) I,$$  \hspace{1cm} (27)

$$\frac{dQ}{dt} = \alpha A - \lambda Q,$$  \hspace{1cm} (28)

$$\frac{dR}{dt} = \alpha I + \mu A - \lambda R,$$  \hspace{1cm} (29)

where $N$ represents the total population and is further divided into five subclasses which include susceptible people $S(t)$, exposed people $E(t)$, infected people $I(t)$, asymptomatic people $A(t)$, and recovered people $R(t)$. The reservoir population is denoted as $Q(t)$.

Since most mathematical models utilize ordinary differential equations with integer order for understanding dynamics of biological systems, every model depending on such classical derivatives has been discovered to have restrictions (Shaikh et al., 2020). These restrictions could be overcome using fractional calculus, as recommended by Caputo and Fabrizio. Researchers such as Shaikh et al. (2020) applied the Caputo-Fabrizio fractional derivative operator to study the dynamics of COVID-19 using the mathematical model suggested by Khan and Atangana (2020) in the form of the system of nonlinear differential equations involving the Caputo–Fabrizio operator (Khan & Atangana, 2020; Shaikh et al., 2020). The model is given as

$$\frac{d^\alpha}{dt^\alpha} S(t) = \Delta - \lambda S - \frac{aS(t) + \beta A(t)}{N} - \gamma SQ,$$  \hspace{1cm} (31)

$$\frac{d^\alpha}{dt^\alpha} E(t) = \frac{S(t) + \beta S(t) I(t)}{N} + \gamma SQ - (1 - \phi) \delta E - \phi \mu E - \lambda E,$$  \hspace{1cm} (32)

$$\frac{d^\alpha}{dt^\alpha} A(t) = (1 - \phi) \delta E - (\sigma + \lambda) I,$$  \hspace{1cm} (33)

$$\frac{d^\alpha}{dt^\alpha} Q(t) = \alpha A - \lambda Q,$$  \hspace{1cm} (34)

$$\frac{d^\alpha}{dt^\alpha} R(t) = \alpha I + \mu A - \lambda R,$$  \hspace{1cm} (35)
With initial conditions

\[ S(0) = \theta_1, E(0) = \theta_2, I(0) = \theta_3, A(0) = \theta_4, R(0) = \theta_5, Q(0) = \theta_6. \]  

Early dynamics of COVID-19 transmission were studied by researchers such as Kucharski et al. (2020), where a combination of a stochastic transmission model with data on both cases in Wuhan and international cases that originated from Wuhan were used to estimate how transmission had varied between January to February 2020. These estimates were then used to calculate the probability of new cases that might generate outbreaks in new areas (Kucharski et al., 2020). Their findings estimated that daily reproduction number, \( R_t \) in Wuhan declined from 2.35 to 1.05 between 1 week before and after travel restrictions were introduced respectively (Kucharski et al., 2020). Based on these estimates, locations with similar transmission potential to Wuhan have at least a 50% chance of an outbreak for very four independently introduced cases (Kucharski et al., 2020).

Several modeling studies have used the SEIR model to study the transmission dynamics of COVID-19. Wu, Leung, and Leung (2020) used the SEIR model to describe the transmission dynamics and forecast the spread of the disease using reported data between December 31, 2019, to January 28, 2020. The study also estimated the basic reproductive number to be 2.68 (Wu, Leung, & Leung, 2020). Another study by Read, Bridgen, Cummings, Ho, and Jewell (2020) using the SEIR model reported a basic reproductive number value of 3.1 using an assumption of Poisson-distributed daily time increments (Read et al., 2020). In contrast, Tang et al. (2020) obtained a basic reproductive number value as high as 6.47 when the clinical progression of the disease, individual epidemiological status, and intervention measures were incorporated into a deterministic compartmental model based on the SEIR model (Tang, Wu, et al., 2020). A different approach was used by Van Zandvoort et al. (2020). An age-stratified SEIR model was used to study the effectiveness of non-pharmaceutical interventions in three African countries (Van Zandvoort et al., 2020). Most African countries have resource-limited settings and have fewer means to suppress virus propagation, and the study observed that isolating infected individuals is the most effective way of reducing transmission in African countries (Van Zandvoort et al., 2020). All these studies are based on the human-to-human transmission and did not take in to account the significance of the environment in COVID-19 transmission (Yang & Wang, 2020). Yang and Wang examined proposed an SEIR model that describes multiple transmission pathways in the infection dynamics. It also emphasized the role of the environmental reservoir in the propagation of COVID-19 (Yang & Wang, 2020). The model employed non-constant transmission rates that change with the epidemiological status and environmental conditions while reflecting the impact of the on-going control measures. Using public data, the study concluded that COVID-19 would remain endemic, and this demands long term prevention and intervention measures (Yang & Wang, 2020).

A different mathematical model approach was employed by Li et al. (2020) where a susceptible–exposed–infectious–quarantined–diagnosed–recovered (SEIQDR) based model, which is an expansion of the SEIR model was used (Li, Wang, et al., 2020). This six-chambered model was used to study the transmission mechanism of COVID-19 and the implemented prevention and control measures, with the aid of time series and kinetic model analysis, a basic reproductive number value of 4.01 was obtained (Li, Geng, et al., 2020). The findings of the study suggested that while recovered individuals might not be re-infected due to the presence of antibodies to COVID-19, bodies of deceased individuals should be well treated to prevent viral transmission (Li, Wang, et al., 2020). Kim et al. (2020) also used a SEIQDR model that factored in behavioral changes to study the transmission of COVID-19 in Korea and predict the likely size and end of the epidemic (Kim et al., 2020). The model predicted over 10,000 cases over time until June, so it was suggested that a sustainable long term non-pharmaceutical interventions would significantly reduce transmission among the population (Kim et al., 2020).

Although the mathematical models for the COVID-19 have majorly forecast few areas relating to pathogen spread such as the basic reproductive number of the SARS-CoV-2, population control measures, percentage of asymptomatic people (Nandal, 2020). There is still a paucity of modeling studies focusing on predicting the magnitude of the global spread of the virus, the duration of the pandemic, and possible effective interventions (Nandal, 2020). Nevertheless, consumers of these models such as the public, media, and politicians; have the need for these predictions to plan for various interventions that would be reliable in combating the disease (Jewell et al., 2020).

Models are very useful tools particularly for short term accurate predictions, and it helps policymakers to make decisions and allocate adequate resources toward disease control through predictions of disease spread and infected population (Kucharski et al., 2020; Revathi & Rangnathan, 2020). Mathematical models can be used to understand how and where the disease is most likely to spread while avoiding so many trial experiments or random guesses with the real population. Most mathematical models used during this epidemic are extensions of the SEIR model, a compartmental model based on the behavior of the population which enabled the simulation of how non-pharmaceutical prevention and intervention measures such as lockdowns, social distancing, self-isolation; can significantly affect the morbidity and mortality of the population over time (Sameni, 2020).

### 4 | CONCLUSION

Although mathematical models mimic the actual reality using an equation that is solved for specific values of the user parameters within the equations, a mathematical model is as good as the data it uses. However, mathematical models are potent tools for understanding the transmission dynamics of an infectious viral disease. In other climes, there is no gainsaying to aver that the SEIR model
seems the most reliable extension of the SIR models during this pandemic due to its plausibility in explaining heterogeneous changes in features, structures, containment and risk analysis of the virus transmission. Since infectious diseases have an incubation period or exposed state in an individual following infection until the symptoms are observed, the SEIR account for the exposed or latent stage which is concomitant with real-time observation across various geography and population. During the COVID-19 Pandemic, mathematical models have played significant roles in policymaking and social life generally. Through various models, different scenarios have been explored to understand the transmission of COVID-19, basic reproductive number, case-fatality rate, duration of epidemic, and significance of various prevention and intervention measures among the population. Although mathematical models rely on predictions and estimations, they are handy tools that could significantly guide the implementation of public health decisions when properly expressed and estimated.

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REFERENCES

Adékunle, I. A., Onanuga, A. T., Akinola, O. O., & Ogbonnjo, O. W. (2020). Modelling spatial variations of coronavirus disease (COVID-19) in Africa. Science of The Total Environment, 729, 138998. http://dx.doi.org/10.1016/j.scitotenv.2020.138998

Bauer, F. (2017). Mathematical epidemiology: Past, present, and future. Infectious Disease Modelling, 2(2), 113–127. https://doi.org/10.1016/j.idm.2017.02.001

Chen, T.-M., Rui, J., Wang, Q.-P., Zhao, Z.-Y., Cui, J.-A., & Yin, L. (2020). A mathematical model for simulating the phase-based transmissibility of a novel coronavirus. Infectious Diseases of Poverty, 9(1), 24. https://doi.org/10.1186/s40249-020-00640-3

Delamater, P. L., Street, E. J., Leslie, T. F., Yang, Y. T., & Jacobsen, K. H. (2019). Complexity of the basic reproduction number (R₀). Emerging Infectious Diseases, 25(1), 1–4. https://doi.org/10.3201/eid2501.179101

Freiberger, M. (2014). Fighting epidemics with maths.plus.maths.org/content/fighting-epidemics-maths

Giordano, G., Blanchini, F., Bruno, R., Colaneri, P., Di Filippo, A., Di Matteo, A., & Colaneri, M. (2020). Modelling the COVID-19 epidemic and implementation of population-wide interventions in Italy. Nature Medicine, 26, 855–860. https://doi.org/10.1038/s41591-020-0883-7

Guo, Y.-R., Cao, Q.-D., Hong, Z.-S., Tan, Y.-Y., Chen, S.-D., Jin, H.-J., ... Yan, Y. (2020). The origin, transmission and clinical therapies on coronavirus disease 2019 (COVID-19) outbreak – An update on the status. Military Medical Research, 7(1), 11. https://doi.org/10.1186/s40779-020-00240-0

Ivorra, B., Ferrández, M. R., Vela-Pérez, M., & Ramos, A. M. (2020). Mathematical modeling of the spread of the coronavirus disease 2019 (COVID-19) taking into account the undetected infections. The case of China. Communications in Nonlinear Science and Numerical Simulation, 88, 105303. https://doi.org/10.1016/j.cnsns.2020.10.5303

Jewell, N., Lewnard, J., & Jewell, B. (2020). Predictive mathematical models of the COVID-19 pandemic underlying principles and value of projections. JAMA, 323, 1893. https://doi.org/10.1001/jama.2020.6585

Khan, M. A., & Atangana, A. (2020). Modeling the dynamics of novel coronavirus (2019-nCov) with fractional derivative. Alexandria Engineering Journal. https://doi.org/10.1016/j.aej.2020.02.033

Kim, S., Seo, Y. B., & Jung, E. (2020). Prediction of COVID-19 transmission dynamics using a mathematical model considering behavior changes. Epidemiology and Health, 42, e2020026. https://doi.org/10.4178/ephid.e2020026

Kucharski, A. J., Russell, T. W., Diamond, C., Liu, Y., Edmunds, J., Funk, S., & Eggo, R. M. (2020). Early dynamics of transmission and control of COVID-19: A mathematical modelling study. Lancet Infectious Diseases, 20, 553–558. https://doi.org/10.1016/S1473-3099(20)30144-4

Li, X., Geng, M., Peng, Y., Meng, L., & Lu, S. (2020). Molecular immune pathogenesis and diagnosis of COVID-19. Journal of Pharmaceutical Analysis, 10(2), 102–108. https://doi.org/10.1016/j.jpha.2020.03.001

Li, Y., Wang, B., Peng, R., Zhou, C., Zhan, Y., Liu, Z., ... Zhao, B. (2020). Mathematical modeling and epidemic prediction of COVID-19 and its significance to epidemic prevention and. Annals of Infectious Disease and Epidemiology, 5(1), 1052.

Lin, Q., Zhao, S., Gao, D., Lou, Y., Yang, S., Musa, S. S., ... He, D. (2020). A conceptual model for the coronavirus disease 2019 (COVID-19) outbreak in Wuhan, China with individual reaction and governmental action. International Journal of Infectious Diseases, 93, 211–216. https://doi.org/10.1016/j.ijid.2020.02.058

Nandal, U. (2020). Mathematical modeling the emergence and spread of new pathogens: Insight for SARS-CoV- and other similar viruses. Pharma R&D Today. Retrieved from https://pharma.elsevier.com/covid-19/mathematical-modeling-the-emergence-and-spread-of-new-pathogens-insight-for-sars-cov-2-and-other-similar-viruses/

Ndairou, F., Area, I., Nieto, J. J., & Torres, D. F. M. (2020). Mathematical modeling of COVID-19 transmission dynamics with a case study of Wuhan. Chaos, Solitons & Fractals, 135, 109846. https://doi.org/10.1016/j.chaos.2020.109846

Panovska-Griffiths, J. (2020). Can mathematical modelling solve the current Covid-19 crisis? BMC Public Health, 20(1), 551. https://doi.org/10.1186/s12889-020-08671-z

Read, M., Bridgen, J., Cummings, D., Ho, A., & Jewell, C. (2020). Novel coronavirus 2019-nCoV: Early estimation of epidemiological parameters and epidemic predictions. Antimicrobial Agents and Chemotherapy, 1–11. https://doi.org/10.1128/AAC.2020.0123.20018549

Revathi, V., & Rangnathan, M. (2020). Why do we need mathematical models for. Web.evolvebio.mp.de.

Sameni, R. (2020). Mathematical modeling of epidemic diseases; a case study of the COVID-19 coronavirus. Aniv, 1–17. http://arxiv.org/abs/2003.11371

Shaikh, A. S., Shaikh, I. N., & Nisar, K. S. (2020). A mathematical model of COVID-19 using fractional derivative: Outcome in India with dynamics of transmission and control. Preprint, 20200401, 1–21. https://doi.org/10.20944/preprints202004.0140.v1

Shil, P. (2016). Mathematical modeling of viral epidemics: A review. Biomedical Research Journal, 3(2), 195. https://doi.org/10.4103/2349-3666.240612

Sinha, D. (2020). Mathematical modeling to estimate the reproductive number and the outbreak size of COVID-19: The case of India and the world. Research Square. https://doi.org/10.21203/rs.3.rs.26261-v1

Tang, B., Wang, X., Li, Q., Bragazzi, N. L., Tang, S., Xiao, Y., & Wu, J. (2020). Estimation of the transmission risk of the 2019-nCoV and its implication for public health interventions. Journal of Clinical Medicine, 9(2), 462. https://doi.org/10.3390/jcm920462

Tang, X., Wu, C., Li, X., Song, Y., Yao, X., Wu, X., ... Lu, J. (2020). On the origin and continuing evolution of SARS-CoV-2. National Science Review, 7, 1012–1023. https://doi.org/10.1093/nsr/nwa036

Torrealba-Rodriguez, O., Conde-Gutiérrez, R. A., & Hernández-Javier, A. L. (2020). Modeling and prediction of COVID-19 in Mexico applying mathematical and computational models. Chaos, Solitons & Fractals, 138, 109946. https://doi.org/10.1016/j.chaos.2020.109946

Van Zandvoort, K., Jarvis, C. I., Pearson, C. A. B., Davies, N. G., Covid, C., Russell, T. W., ... Liu, Y. (2020). Response strategies for COVID-19
epidemics in African settings: A mathematical modelling study. London: Centre for Mathematical Modelling of Infectious Diseases.

WHO. (2020). Coronavirus disease 2019 (COVID-19) situation Report-68. Geneva: World Health Organization.

Wu, A., Peng, Y., Huang, B., Ding, X., Wang, X., Niu, P., ... Jiang, T. (2020). Genome composition and divergence of the novel coronavirus (2019-nCoV) originating in China. Cell Host & Microbe, 27(3), 325–328.

Wu, J., Leung, K., & Leung, G. (2020). Nowcasting and forecasting the potential domestic and international spread of the 2019-nCoV outbreak originating in Wuhan, China: A modelling study. Lancet, 395(10225), 689–697.

Yang, C., & Wang, J. (2020). A mathematical model for the novel coronavirus epidemic in Wuhan, China. Mathematical Biosciences and Engineering, 17(3), 2708–2724.

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