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The XMM – Newton Ω project: III. Gas mass fraction shape in high redshift clusters

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Abstract. We study the gas mass fraction behavior in distant galaxy clusters observed within the XMM – Newton Ω project. The typical gas mass fraction $f_{\text{gas}}$ shape of high redshift galaxy clusters follows the global shape inferred at low redshift quite well, once scaled appropriately: the gas mass fraction increases with radius and flattens outward. This result is consistent with the simple picture in which clusters essentially form by gravitational collapse, leading to self similar structures for both the dark and baryonic matter. However, we find that the mean gas profile in distant clusters shows some differences to local ones, indicating a departure from strict scaling. Assuming an Einstein-de Sitter cosmology, we find a slight deficit of gas in the central part of high-$z$ clusters. This result is consistent with the observed evolution in the luminosity-temperature relation. We quantitatively investigate this departure from scaling laws by comparing $f_{\text{gas}}$ from a sample of nearby galaxy clusters (Vikhlinin, Forman & Jones, 1999) to our eight high-$z$ clusters. Within the local sample, a moderate but clear variation of the amplitude of the gas mass fraction with temperature is found, a trend that weakens in the outer regions. Taking into account these variations with radius and temperature, the apparent scaled gas mass fractions in our distant clusters still systematically differ from local clusters. This reveals that the gas fraction does not strictly follow a scaling law with redshift. This provides clues to understand the redshift evolution of the $L–T$ relation whose origin is probably due to non-gravitational processes during cluster formation. An important implication of our results is that the gas fraction evolution, a test of the cosmological parameters, can lead to biased values when applied at radii smaller than the virial radius. From our XMM clusters, as well as Chandra clusters in the same redshift range, the apparent gas fraction at the virial radius obtained by extrapolation of the inner gas profile is consistent with a non-evolving universal value in a high matter density model while in a concordance, model high redshift clusters show an apparent higher $f_{\text{gas}}$ at the virial radius than to local clusters.

1. Introduction

Clusters of galaxies are unique cosmological probes whose statistical properties represent major sources of information for understanding the history of structure formation as well as for the determination of the cosmological parameters. X-ray observations are particularly relevant in this perspective as they allow one to estimate the distribution of both the baryonic and total mass components, a rather unique situation when studying structures in cosmology. In the simplest picture of purely gravitationally-driven formation of virialized systems like galaxy clusters, it is expected that such objects exhibit self-similarity (Kaiser 1986). In this model physical properties of galaxy clusters obey scaling laws which naturally emerge from the fact that there is no preferred scale and therefore two clusters of different masses should have identical internal structure.
We base our analysis on the XMM data obtained on a sample of eight distant clusters observed as part of the \textit{XMM–Newton $\Omega$} project, a systematic \textit{XMM–Newton} guaranteed time follow-up of the most distant SHARC clusters (Bartlett et al. 2002). The high sensitivity of \textit{XMM–Newton} allows us to investigate emissivity in high redshift clusters beyond half the virial radius, a remarkable result (Arnaud et al. 2002). Our sample represents an homogeneous sample of eight bona fide clusters with median luminosities between 2 and 15 $10^{44}$ erg/s (in an Einstein de Sitter cosmology with a Hubble constant of 50 km/s/Mpc) with redshifts in a relatively restricted range, between 0.45 and 0.65. This sample is therefore expected to be fairly representative of the cluster population at high redshift, allowing a systematic analysis of the gas mass profiles and therefore allowing us to address the issue of gas mass fraction self-similarity and its implications in constraining the cosmological parameters. Moreover, the high sensitivity of \textit{XMM–Newton} makes possible a statistical investigation of the outer gas distribution in this sample, a key aspect as we will see. The detailed data reduction and analysis of this sample is presented in Lumb et al. (2004). The present paper is organized as follows. In section 2 we discuss the expectation of the gas mass fraction from scaling arguments as well as the results of the comparison of gas mass fraction in distant clusters to low redshift ones. In section 3, we discuss the consequence of our findings for the use of clusters as cosmological probes. Finally, our conclusions are given in section 4. We used a Hubble constant of 50 km/s/Mpc unless the dependence is explicitly given (with $H_0 = 100$ km/s/Mpc).

2. Scaling properties

Self-similar assumptions imply that the radial profile of any physical quantity should exhibit a similar shape independently of the cluster mass and at any redshift, once normalized to the virial radius. Numerical simulations in which only gravitational physics is taken into account indicate that halos of different masses follow a universal density profile, the so-called NFW profile (Navarro, Frenk & White 1996). On the observational side, the X-ray emissivity profiles in hot galaxy clusters have been also found to be very similar, at least in the outer part (Porron et al. 1999; Neumann & Arnaud 1999, 2001). Furthermore, evidence has been found that radial profiles of the $f_{\text{gas}}$, as well as the baryon fraction $f_b$, are similar and seem to follow a roughly universal shape (Roussel et al. 2000, hereafter RSB00). It has been found that such a universal profile is in reasonable agreement with the predictions of numerical simulations (Sadat & Blanchard 2001; hereafter SB01). This supports the idea that the gas structure has not been strongly disturbed by non-gravitational processes and supports the principle of using their properties to constrain cosmological parameters.

Previous studies of the baryonic content in clusters indicated that baryons contribute 15-20% of the total cluster mass (for $h = 0.5$); if the baryon fraction $f_b = M_b/M$ is representative of the universe as a whole and, provided that the actual baryon abundance is known, the cosmological matter density parameter $\Omega_M$ should lie in the range $\Omega_b/f_b = 0.2 - 0.5$ (White et al.
Fig. 1. Apparent $f_{\text{gas}}$ plotted versus radius normalized to the virial radius $R/R_V$. The left side corresponds to $f_{\text{gas}}$ in an Einstein-de Sitter model and the right side to the concordance model. In the upper graphs, the lines show the individual clusters $f_{\text{gas}}$ up to the maximum radius of detection (see Lumb et al. 2004), dots correspond to extrapolated $f_{\text{gas}}$. The data (red and purple circles) are the $f_{\text{gas}}$ in local sample (from RSB00 for the inner part and from VFJ99 in the outer parts) in an Einstein de Sitter cosmology and in a flat low density model. The error bars correspond to the typical dispersion in the VFJ99 sample. In the lower graphs, the average apparent $f_{\text{gas}}$ and its uncertainty are plotted (filled area).

1993, David et al. 1995, Evrard 1997). However, although the gas mass fraction profile follows quite well the self-similarity assumption (RSB00), the density parameter derived from the baryon fraction estimation might be corrupted by different effects that are related to the internal structure of the gas and that could alter the inferred value (SB01).

2.1. Estimation of the cluster $f_{\text{gas}}$ under the scaling hypothesis

As already mentioned, the self-similarity hypothesis implies that the spatial variation of any physical quantity depends solely on $R/R_V$: the virial radius $R_V$ can be obtained from its definition $M_A = 4/3\pi(1 + \Delta_v)(1 + \Delta_v)R_V^3$:

$$R_V = 1.34 M_{15}^{2/3}(\Omega_0(1 + \Delta_v)/179)^{1/3}h^{-2/3}(1 + z)^{-1}(h^{-1}\text{Mpc})$$

where $\Delta_v$ is the virial contrast density compared to the universe. In an Einstein-de Sitter universe, one has $\Delta_v = 18\pi^2$. In other cosmological models, there is some ambiguity as to how to define the proper reference radius for scaling relations. Commonly, the virial radius is defined from the spherical top-hat model (see for instance Bryan & Norman, 1998; note that these authors provide useful fits to compute $\Delta_v$ with formulæ involving $\Delta_v$, the contrast density, compared to a critical universe of density $\rho_c(z) = 3H(z)^2/8\pi G$). The scaling of the mass-temperature relation is then obtained from $T \propto GM/R_V$:

$$T = A_{TM} M_{15}^{2/3}(\Omega_0(1 + \Delta_v)/179)^{1/3}h^{-2/3}(1 + z)\text{keV}$$

The normalization $A_{TM}$ can be obtained from numerical simulations (Evrard, Metzler, Navarro 1996, Bryan & Norman 1998) or inferred from observations. In the following, we use the same calibration as in SB01, $A_{TM} = 5.86$, allowing a direct comparison with their results. Several studies have been performed in order to test the $M_V$–$T$ relation as predicted from numerical simulations by means of X-ray observations (see e.g. Horner et al. 1999, Nevalainen et al. 2000, Finoguenov et al. 2001, Sanderson et al. 2003). Disagreements have been found concerning both the normalization $A_{TM}$ and the slope (steeper than the predicted 1.5) for cooler systems ($T_X$ less than 4 keV). Note however that different normalizations $A_{TM}$ of the $M_V$–$T$ relation are not expected to make a difference in the comparison between local and high redshift samples, therefore the $f_{\text{gas}}$ test is essentially based on the assumption that scaling of the $M_{\text{gas}}$–$T$ relation is correct. The gas mass fraction at a given radius $f_{\text{gas}}(r) =$
\(M_{\text{gas}}(r)/M_{\text{tot}}(r)\) is computed for each cluster. The gas mass profile follows directly from the electron number density profile:

\[
M_{\text{g}}(r) = 4\pi \frac{m_p}{1 - Y/2} \int_0^r n_e(r') r'^2 dr',
\]

where \(Y\) is the helium mass fraction (hereafter \(Y = 0.25\)). We assume a fully ionized gas, spherically distributed, and a \(\beta\)-model for its distribution, which is known to provide a good representation of the gas out to the outer regions (VF99):

\[
n_e(r) = n_e(0) \left(1 + \left(\frac{r}{r_c}\right)^2\right)^{-3\beta} \tag{4}
\]

where \(r_c\) and \(\beta\) corresponding to the best fit values derived in Lumb et al. (2004). The central gas density \(n_e(0)\) was derived from the normalization \(K\) of the XSPEC Mekal model defined by

\[
K = \frac{10^{-14}}{4\pi(D_d \times (1+z))^2} \int n_e n_p dV.
\]

where \(n_e\) and \(n_p\) are respectively the electron and proton number densities and \(D_d\) is the angular distance to the cluster. We assume \(n_p = 0.82 n_e\) in the ionized intra-cluster plasma. The emission integral \(E1 \propto \int n_e n_p dV\) was evaluated assuming that the x-ray emission extends up to the virial radius, in order to be fully consistent with Lumb et al. (2004). There is some arbitrariness in the assumption of the radius up to which the emission has to be taken into account, ranging from the largest radius at which the emission is detected up to infinity. For our sample, the contribution to the flux of the emission, estimated by extrapolation of the fitted profile, beyond the detection radius is less than 1%, and therefore represents a negligible source of uncertainty on our derived gas masses.

The normalization \(K\) value of each cluster was taken from Table 2 of Lumb et al. (2004).

The dark matter profile was assumed to follow the NFW analytical profile (Navarro et al. 1996) with a concentration parameter \(c = 5\) in order to allow direct comparison with RSB00 (again, changing the value of the concentration parameter is not expected to modify the relative comparison of local and distant clusters).

In this study we will consider two cosmologies: an Einstein-de-Sitter (EdS) Universe (\(\Omega_m = 1\)) and a concordance model (\(\Lambda\)CDM) Universe with (\(\Omega_m = 0.3, \Omega_\Lambda = 0.7\)). The apparent \(f_{\text{gas}}\) values of our \(\text{XMM} - \text{Newton}\) clusters estimated at \(r_{500}\) are given in Table 2 for both cosmologies. The mean \(f_{\text{gas}}\) value at \(r_{500}\) is \(f_{\text{gas}} = 0.095\) in an EdS model and \(f_{\text{gas}} = 0.14\) in a \(\Lambda\)CDM model.

### 2.2. The shape of the apparent gas mass fraction

In order to investigate the global shape of \(f_{\text{gas}}\) profile we have followed the procedure similar to RSB00. We compute \(f_{\text{gas}}\) up to the maximum radius of detection (published in Lumb et al. 2004). Beyond this limit, this limit \(f_{\text{gas}}\) is obtained by extrapolating up to the virial radius. The radial distribution in the local sample is derived using the published \(f_{\text{gas}}\) values up to the X-ray limiting radius \(R_{\text{x,lim}}\) (RSB00), upward of this radius we computed \(f_{\text{gas}}\) at the two fiducial radii \(R_{1000}\) and \(R_{2000}\) defined by Vikhlinin, Forman & Jones (1999, hereafter VF99) for which they published the gas masses \(M_g = 4/3\pi n_p(1 + \Delta)R_s^3 (1 + z)^3\), allowing a comparison in the most outer regions. For this comparison we do not correct for clumping (Mathiesen et al. 1999) as the radial variation of this quantity is unknown. Moreover, if the scaling holds, the emission of both local and distant clusters should be biased by the same amount by this effect, still allowing a meaningful direct comparison.

The scaled \(f_{\text{gas}}\) radial profiles of the individual high-z clusters and the mean \(f_{\text{gas}}\) profile of the local sample derived for both EdS and \(\Lambda\)CDM models are displayed in Fig. 4. For a given value of the normalization \(\sigma_T M\), the virial radius (for a given temperature) depends on the cosmology through equation 1 and 2. However, in practice for a NFW profile the masses inferred in a fixed physical radius for low redshift clusters are very similar in both cosmologies. As expected, a noticeable difference in the amplitude of \(f_{\text{gas}}\) in distant clusters appears, depending on the cosmological model. For both cosmological models, the scaled \(f_{\text{gas}}\) profile of distant clusters is globally in good agreement with what has been inferred for clusters at low redshift by SB01: the apparent mean gas profile of our distant clusters increases from the center to outer shells following roughly a universal gas mass fraction shape. Interestingly, these \(f_{\text{gas}}\) exhibit a level of dispersion consistent with what has been found previously (RSB00, VF99). In the EdS model the most central values of \(f_{\text{gas}}\) seem smaller in high redshift clusters. Such a deviation is consistent with the measured evolution of the \(L_X - T_x\) relation, weaker than expected if the scaling strictly hold. Conversely, in the low density flat model, \(f_{\text{gas}}\) values in the central parts of distant clusters seem to agree more with the scaling, again in agreement with the evolution of the \(L_X - T_x\) relation in this cosmology. However, in the outer regions the mean \(f_{\text{gas}}\) in the \(\text{XMM} - \text{Newton}\) distant sample seems not to match the local one very well. Examination of the average \(f_{\text{gas}}\) compared to the local one more clearly reveals a systematic difference: the inner mean gas mass fraction in distant clusters does not rise as rapidly as in the local sample. It is unclear whether this difference is real, given the various origins of clusters used in the local sample.

### 2.3. \(f_{\text{gas}} - T_x\) correlation

In order to understand whether the above difference is meaningful, an accurate knowledge of the gas mass fraction is needed. By examination of the RSB01 sample, restricted to clusters for which the actual X-ray extension was known, we found a clear trend of \(f_{\text{gas}}\) increasing with temperature (this trend is much less clear in the global sample). However, this sample was not designed to offer a uniform sample for X-ray studies, therefore it has been used only as a guideline in the present study. To examine in a more systematic and uniform way whether \(f_{\text{gas}}\) varies with temperature, we have computed \(f_{\text{gas}}\) of nearby clusters at the two fiducial radii \(R_{2000}\), \(R_{1000}\) used in VF99 as well as the virial radius. The gas mass fraction in our high-z cluster sample has been estimated at the same aver-
Table 1. Apparent gas mass fractions at $r_{500}$ in both EdS and ΛCDM cosmologies with $h = 0.5$, uncorrected for clumping, with uncertainties from temperature uncertainties. Temperature measurements are taken from Lumb et al. (2004) without cooling flow excision.

| Cluster name | RXJ0337.7 | RXJ0505.3 | RXJ0847.2 | RXJ1120.1 | RXJ1325.5 | RXJ1334.3 | RXJ1354.2 | RXJ1701.3 |
|--------------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| $z$           | 0.577     | 0.51      | 0.56      | 0.60      | 0.445     | 0.62      | 0.551     | 0.45      |
| $T$ (keV)     | 2.6       | 2.5       | 3.62      | 5.45      | 4.15      | 5.2       | 3.66      | 4.5       |
| $r_{500}$ (EdS) | 0.723     | 0.757     | 0.867     | 1.024     | 1.041     | 0.982     | 0.879     | 1.079     |
| $f_{\text{gas}}$ (EdS) | 0.0782$^{+0.0000}_{-0.0010}$ | 0.0987$^{+0.0011}_{-0.0009}$ | 0.0959$^{+0.0005}_{-0.0015}$ | 0.1054$^{+0.0006}_{-0.0005}$ | 0.0703$^{+0.0005}_{-0.0005}$ | 0.095$^{+0.0005}_{-0.0005}$ | 0.1162$^{+0.0012}_{-0.0013}$ | 0.1016$^{+0.0025}_{-0.0023}$ |
| $r_{500}$ (ΛCDM) | 1.315    | 1.358     | 1.572     | 1.87      | 1.843     | 1.799     | 1.591     | 1.911     |
| $f_{\text{gas}}$ (ΛCDM) | 0.1109$^{+0.0014}_{-0.0015}$ | 0.1500$^{+0.0018}_{-0.0014}$ | 0.1431$^{+0.0021}_{-0.0025}$ | 0.1495$^{+0.0009}_{-0.0007}$ | 0.1007$^{+0.0007}_{-0.0007}$ | 0.1446$^{+0.0009}_{-0.0007}$ | 0.1825$^{+0.0025}_{-0.0022}$ | 0.1424$^{+0.0038}_{-0.0034}$ |

Table 2. Least square fit of the gas fraction to the local sample of x-ray clusters. Uncertainty in the normalization constant is 4-5%. The dispersion around the fit is also given in percent.

| Radius   | Gas fraction ($\Omega_m = 1$) | Gas fraction ($\Omega_m = 0.3$) |
|----------|-------------------------------|-------------------------------|
| $R_{2000}$ | 0.061$^{+0.040}_{-0.005}$ (17%) | 0.063$^{+0.040}_{-0.005}$ (16%) |
| $R_{1000}$ | 0.075$^{+0.030}_{-0.015}$ (17%) | 0.075$^{+0.030}_{-0.015}$ (17%) |
| Virial    | 0.090$^{+0.020}_{-0.015}$ (18.8%) | 0.0977$^{+0.018}_{-0.018}$ (22%) |

tual variation of $f_{\text{gas}}$ in clusters, but it might also be due to a variation of the clumping of the gas with temperature. The XMM distant sample does not reveal any clear trend with temperature, due to its limited temperature range. However, when combined with Chandra clusters, a sequence appears similar to the one observed in local clusters. Comparison of the high-$z$ $f_{\text{gas}}$ at $R_{1000}$ and $R_{2000}$ radii reveals that this internal structure also varies with redshift: the observed mean $f_{\text{gas}}$ profile of distant clusters seems to increase toward the outer part less rapidly than in local clusters. This introduces an additional degree of complexity when it comes to the description of the scaling predictions. Indeed if the gas mass fraction varies with $T$, scaling would imply:

$$f_{\text{gas}}(R/R_v, T, z) = f_{\text{gas}}(R/R_v, T \times T_*(0)/T_*(z), z = 0)$$

(6)

where $T_*(z)$ is the characteristic temperature associated with a characteristic mass scale at the epoch $z$ (defined by $\sigma(M_*, z) = \text{constant}$). Therefore, we plot the predicted variations of $f_{\text{gas}}$ under this scaling assumption. Comparing predictions from this scaling scheme at the three different radii shows that the variations with redshift of the internal structure do not follow the scaling either. This is a clear indication that clumping arising from hierarchical building of clusters in a purely gravitational picture is not the only origin of the observed complexity. Rather, it is likely to originate from non-gravitational heating processes, whose modifications of the internal structure of clusters are not expected to follow standard scaling. It is interesting to note that at the virial radius, the $f_{\text{gas}}$ values we obtained for XMM and Chandra clusters are consistent and suggest that the gas fraction may not vary any longer with temperature. As our gas quantities are extrapolated beyond emission detection (although not by much, especially in the case of the Chandra clusters), it would be important to have deeper observations of the outer regions of clusters to confirm this result, both for local and distant clusters.

Finally we have also considered another possibility. Vauclair et al. (2003) have shown that the concordance model
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**Fig. 2.** $f_{\text{gas}}$ versus temperature at three different radii $R_{2000}$ (top), $R_{1000}$ (middle) and $R_v$ (bottom) in the outer parts of the XMM – Newton distant clusters (blue squares and red crosses) in Einstein de Sitter model (on the left) and in a concordance model (crosses on the right side) compared to the same quantity (plus symbols) evaluated at the same scaled radii from the local sample by VFJ99. Open (green) squares and small (green) crosses are the same quantities evaluated for clusters in the Vikhlinin’ sample (Vikhlinin et al., 2002) within the same redshift range ($0.4 < z < 0.62$). Errors bars (coming from the uncertainty on the temperature) have been drawn in one case ($R_{1000}$). In the concordance case, standard scaling of the mass–temperature relation leads to gas fractions represented by the (red) crosses. Dashed (colored) lines are the expected $f_{\text{gas}}$ at the fiducial redshift of the XMM – Newton clusters from scaling relations.

when properly normalized to local cluster abundances, could not reproduce the observed numbers counts of distant clusters unless the mass temperature scaling with redshift is modified:

$$T = A_{TM}M_1^{2/3}(\Omega_0(1 + \Delta_v)/179)^{1/3}h^{2/3} \text{ keV}$$  

(7)

(i.e. the $(1 + z)$ term in Eq. [2] has been removed). This changes the apparent gas mass fraction in distant clusters as well as the predictions of the scaling model. The gas mass fractions on both low and high redshift clusters were recomputed, as was the expected scaled variation of $f_{\text{gas}}$ with temperature. The results are shown as green symbols and lines in the colored version of Figure 2. Again, the scaling hypothesis seems not to work well under this scheme, perhaps not surprisingly given that the scaling has been already abandoned.

3. Cosmological application

The idea that the actual $f_{\text{gas}}$ in clusters should be universal is the starting point of an interesting cosmological test that has been proposed based on the apparent evolution of $f_{\text{gas}}$ with redshift (Sasaki 1996; Pen, 1997; Cooray 1998). The principle of this test is based on the fact that the inferred gas mass fraction from
X-ray data depends on the assumed cosmology through the angular distance. Comparing the high redshift value to what is inferred from local clusters provides us in this way with a new test to constrain the cosmological parameters.

However, from our study, it appears that there are several sources of complexity when applying this test. A first fact that should be taken into account is that \( f_{\text{gas}} \) varies with radius inside clusters. This variation can be accommodated if the shapes are self-similar, by working at identical scaled radius, i.e. \( R/R_\text{c} = \) constant (or in a nearly equivalent way, at similar density contrast). Clearly, in order to prevent any bias one should compare \( f_{\text{gas}} \) at identical radii (in units of virial radius) up to which gas emission is detected. The second problem is that the apparent \( f_{\text{gas}} \) has been found to vary with temperature (mass). There has been some debate on the strength of this effect (David et al 1995, Arnaud & Evrard 1999, Mohr et al 1999, RSB00), but such a possibility should be kept in mind when applied to cosmological purposes. What we have obtained from the analysis of the VFJ99 sample is that in the inner part of clusters both the shape and the amplitude of the gas mass fraction varies with temperature. In such a regime, it is unclear whether arguments based on the scaling hypothesis are valid. However, our result are consistent with the hypothesis that the gas fraction is constant at the virial radius. It is therefore vital to have better data on the \( f_{\text{gas}} \) behavior in clusters in their outer part, in order to reach conclusions of cosmological relevance.

The fact that the dispersion in \( f_{\text{gas}} \) measurements in our distant sample is similar to that obtained in local clusters is very positive. Indeed, uncertainties on \( f_{\text{gas}} \) (from uncertainties on temperature and flux) in our distant clusters are significantly smaller than the intrinsic scatter (see Fig 2). From our study it appears that although the global \( f_{\text{gas}} \) shape in distant clusters is similar to the shape obtained at low redshift, the complex internal structure, i.e. the variation of the gas mass fraction with radius, with temperature and with redshift reveals differences that cannot be described in a simple scalable scheme. The observed variations in the central parts are clear indications that \( f_{\text{gas}} \) evolution argument cannot be used in this regime, given the present (lack of) understanding of the gas physics in clusters. However, the fact that \( f_{\text{gas}} \) appears to be almost constant against temperature at the virial radius is an important piece of information indicating that the argument of a non-evolving \( f_{\text{gas}} \) could be valid at this radius. From Fig. 2, we can see that \( f_{\text{gas}} \) derived from XMM – Newton clusters as well as from Chandra clusters are consistent with the values obtained in low redshift clusters for the EdS model, while we observe a clear offset between \( f_{\text{gas}} \) values in distant and nearby clusters computed in the case of a ΛCDM model. The concordance model under the assumption of standard scaling has been found to be ruled out at a level of significance of more than 4 \( \sigma \) from the XMM data (6 \( \sigma \) when combined with Chandra measurements) while the Einstein–de Sitter model lies at better than 1 \( \sigma \).

Several aspects however make the direct cosmological interpretation difficult. First our sample is quite small and it would be invaluable to have an extended version with a significantly larger number of clusters. However, the fact that similar results are obtained from the Chandra data is very encouraging. As a trend has been found with temperature, it is possible that similar trends exist with luminosity. Therefore meaningful statistical comparisons require data from X-ray selected cluster samples and as much as possible from comprehensive analysis. The second point is that a clear trend with temperature exists and could be a source of confusion: temperatures in our sample are lower than in the local sample and therefore expected average \( f_{\text{gas}} \) values are smaller (for the same \( R/R_\text{c} < 1 \)). Comparing \( f_{\text{gas}} \) in our clusters with the hottest local cluster, would have led to a systematic bias, at least for the inner regions. Indeed, it is expected that the brightest clusters (at a fixed temperature and at a given redshift) would have a higher inner baryon fraction than the average population. Therefore it is natural that the trend observed with temperature is also present with luminosity. Finally, we showed that the internal structure of the gas is not strictly identical in high and low redshift clusters, declining faster in the central part of high redshift clusters. This is consistent with what seems already to emerge from Fig. 1. This complex internal structure is probably the result of non-gravitational (pre) heating of the gas which is currently advocated to explain the observed \( L_X – T \) relation, but might also result from more fundamental

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**Fig. 3.** Same quantities as in Figure 2. Light grey (green) crosses were obtained for a concordance model assuming the non-standard scaling \( M_\text{v} – T \) relation from Vauclair et al (2003), Eq. 4. The dotted (green) line is the expectation from scaling in this case. Left side is at \( (R_{2000}) \), right side is at the virial radius.
departure of scaling laws in the dark matter, for instance if $c$ evolved with redshift. These systematic variations with radius, temperature and redshift imply that the baryon fraction test should be performed with caution and probably only at the virial radius, although one expects that outer regions are more affected by clumping and it is not clear that clumping should follow simple scaling relations in a low density universe.

4. Conclusion

The observations of distant clusters with $XMM-Newton$ offer an unique possibility to investigate the outer emissivity of the gas distribution in distant X-ray clusters. These observations have revealed for the first time the existence of a complex internal structure which does not follow simple scaling laws but still does show some regularities. The $XMM-Newton$ observations of the distant SHARC clusters reveal some interesting results on this issue: the shape of the apparent $f_{\text{gas}}$ derived for these clusters is in good agreement with the shape inferred by SB01 for local clusters. This is an independent confirmation that the scaled shape of the gas mass fraction in clusters is in rough agreement with numerical simulations. However, our analysis reveals some deviations from the standard scaling in the $f_{\text{gas}}$ profile of high redshift clusters. Furthermore, by comparing our distant clusters to a sequence of local clusters, we found a clear variation of the internal structure with temperature and redshift which cannot be described by simple scaling relations. This implies that the baryon fraction evolution, or lack thereof, cannot be used as a reliable cosmological test without better understanding of the internal structure of clusters. Nevertheless, at the virial radius the gas fraction seems to be independent of temperature in the low redshift sample and therefore that the high-redshift clusters might be used to apply the cosmological test based on the assumption that $f_{\text{gas}}$ at the virial radius has a universal value independent of redshift, although existing data do not allow a firm statement about this hypothesis. From our sample of high redshift clusters at the virial radius the data are found to be roughly consistent with a non-evolving $f_{\text{gas}}$ in an Einstein-de Sitter model, but not within the standard concordance model in which the inferred apparent $f_{\text{gas}}$ appears systematically higher than in local clusters, unless a non-standard scaling with redshift of the $M$–$T$ relation (Vauclair et al. 2004) is used. However, the complex internal structure of the gas revealed by the present analysis of $XMM-Newton$ clusters prevents us from drawing definitive conclusions on cosmological parameters, as the relevant quantities were extrapolated at the virial radius. In the concordance model the mean $f_{\text{gas}}$ value estimated inside the radius of detections, is still found to lie at $4\sigma$ above the mean gas mass fraction of nearby clusters with similar temperature.

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