Large Faraday effect and structural properties of heavily Tb\textsuperscript{3+}-doped borogermanate glasses: a potential precursor of magneto-optical fibers

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Abstract

New glass compositions containing high concentrations of Tb\(^{3+}\) ions were developed aiming at the production of magneto-optical (MO) fibers. This work reports on the structural and MO properties of a new glass composition based on \((100-x)(41\text{GeO}_2\text{-25B}_2\text{O}_3\text{-4Al}_2\text{O}_3\text{-10Na}_2\text{O}\text{-20BaO}) - x\text{ Tb}_4\text{O}_7\). Morphological analysis (HR-TEM) of the sample with the highest concentration of Tb\(^{3+}\) ions confirmed the homogeneous distribution of Tb\(^{3+}\) ions and the absence of nanoclusters. All the samples presented excellent thermal stability against crystallization (\(\Delta T > 100 \degree C\)). An optical fiber was manufactured by a fiber drawing process. The UV-Vis spectra of the glasses showed Tb\(^{3+}\) electronic transitions and optical windows varying from 0.4 to 1.6 \(\mu m\). The magneto-optical properties and the paramagnetic behaviors of the glasses were investigated using Faraday rotation experiments. The Verdet constant (\(V_B\)) values were calculated at 500, 650, 880, 1050, 1330, and 1550 nm. The maximum \(V_B\) values obtained at 650 and 1550 nm for the glass with \(x = 18\) mol\% were -128 and -17.6 rad T\(^{-1}\) m\(^{-1}\), respectively. The \(V_B\) values at 500 and 1550 nm for the optical fiber containing 8 mol\% of \(\text{Tb}_4\text{O}_7\) were -110.2 and -9.5 rad T\(^{-1}\) m\(^{-1}\), respectively, while the optical loss at around 880 nm was 6.4 dB m\(^{-1}\).

Introduction

Magneto-optical (MO) materials based on the Faraday effect have been increasingly studied for use in new technologies\(^{1,2}\). MO materials have been applied as modulators, as optical isolators, and as magneto-optical fiber sensors\(^{3-5}\). A wide variety of transparent MO glasses, crystals, and transparent glass-ceramics containing rare earth (RE) ions such as Tb\(^{3+}\), Dy\(^{3+}\), Pr\(^{3+}\), and Gd\(^{3+}\) have been investigated and are considered promising materials for photonics and spintronics\(^{6-8}\).

The Faraday effect is defined by the rotation angle (\(\theta\)) of a linearly polarized light beam, when the light travels through an optical path of known length (\(l\)), under the application of a longitudinal magnetic field (\(B\)) along the light propagation direction\(^9\). The MO performance of a material is evaluated and quantified by the magnitude of the Verdet constant (\(V_B\)) value, and it may be maximized by the incorporation of paramagnetic species\(^10\).

Single crystals have larger \(V_B\) values than magneto-optical glasses with similar composition. However, MO materials produced from glasses are more attractive than crystals, due to their lower cost, isotropy, and simple preparation procedures, in addition to great flexibility in obtaining materials with different shapes and lengths, such as fibers for applications in integrated devices\(^11\). Among the MO materials, especially attractive are
paramagnetic glasses containing high concentrations of Tb$^{3+}$ ions and with large $V_B$ values in UV-Vis-NIR regions$^{12,13}$.

The development of MO glass compositions able to support high RE ions contents and with high thermal stability represents an important step towards achieving successful fiber drawing processes without crystallization. Studies have reported the production of MO fibers based on Pr$^{3+}$-doped aluminosilicate$^{14}$, Eu-doped silica glass$^{15}$, Gd$_2$O$_3$ NPs-doped aluminosilicate glass$^{16}$, and Tb$^{3+}$-doped silicate glasses$^{17}$.

The main prerequisites in selection of a good candidate glass material for MO applications are large $V_B$ values and transparency in the visible and near-infrared (NIR) regions. In particular, for the NIR region (at 1550 nm), MO materials are good options for applications in telecommunication systems. Among all the paramagnetic ions, Tb$^{3+}$ is one of the most attractive$^{1,13,18}$. It has the electronic configuration $4f^8 \rightarrow 4f^7 5d^1$, providing good paramagnetic behavior and among the highest magnetic moments ($\mu_{\text{eff}} = 9.5-9.72$) and susceptibilities ($J = 6, g = 1.46$) of all the rare earth ions$^1$. Additionally, terbium gallium garnet single crystals (Tb$_3$Ga$_5$O$_{12}$), known as TGG, are available commercially and are considered one of the most important bulk MO materials, with $V_B$ of -134 rad T$^{-1}$ m$^{-1}$ at 632 nm$^{19}$. Currently, heavy metal oxide (HMO) glasses based on borogermanates and borate glasses containing high Tb$^{3+}$ ions contents stand out, due to their large $V_B$ values in the red region of the visible spectrum$^{13}$. Gao et al.$^1$ reported the MO properties of heavily Tb$^{3+}$-doped materials with large Verdet constant values for use in fiber-integrated magneto-optics. In this case, the highest $V_B$ (at 632.8 nm) was -119 rad T$^{-1}$ m$^{-1}$ for glass containing 25 mol% of Tb$_2$O$_3$. Franco et al.$^{20}$ reported MO glasses based on the GeO$_2$-B$_2$O$_3$-Al$_2$O$_3$-Na$_2$O-PbO-Tb$_4$O$_7$ composition, with maximum $V_B$ values at 650 and 1550 nm equal to -83.9 and -15.5 rad T$^{-1}$ m$^{-1}$, respectively, for a sample containing 8 mol% of Tb$_2$O$_7$ (35 wt% of Tb dopant). In addition, the authors showed the production of an MO fiber from the drawing process of a glass containing 4 mol% of Tb$_2$O$_7$. Yin et al.$^{13}$ reported the structural and MO properties of 20Tb$_2$O$_3$-20Ga$_2$O$_3$-xB$_2$O$_3$-(35-x)SiO$_2$-20GeO$_2$ (20 ≤ x ≤ 35) glasses. In this case, the authors reported the variation of $V_B$ values at 450 nm (from -210 to -236 rad T$^{-1}$ m$^{-1}$), as a function of B$_2$O$_3$ content. Guo et al.$^{21}$ showed that the $V_B$ values (at 632.8 nm) of GeO$_2$-B$_2$O$_3$-SiO$_2$-Ga$_2$O$_3$-xB$_2$O$_3$ (15 ≤ x ≤ 30) glasses ranged from -49.98 to -120.54 rad T$^{-1}$ m$^{-1}$, with increase of the Tb$_2$O$_3$ content. Suzuki et al.$^{12}$ reported large Faraday effects in bulk borate glasses containing Tb$_2$O$_7$ (45, 55, and 60 mol%). The large Verdet constant values for these Tb$^{3+}$-borate glasses (at 633 nm) were -172, -212, and -234 rad T$^{-1}$ m$^{-1}$, respectively$^{12}$. Savinkov et al.$^{22}$ described the MO properties of transparent and colorless Tb$_2$O$_3$-B$_2$O$_3$-GeO$_2$ (TBG) glasses containing up to 33 mol% (or
12.13 x 10^{-21} \text{ion cm}^{-3} \text{)} \text{ of \ T}_2\text{O}_3. \text{ The maximum } V_B \text{ value obtained at 632.8 nm was -0.409 arc min cm}^{-1} \text{ Oe}^{-1} \text{ (~ -119 rad T}^{-1} \text{ m}^{-1}). \text{ As mentioned above, the literature includes very interesting works concerning MO characterization of bulk HMO glasses containing RE oxides, but very few papers have addressed MO fiber production}^{17,20,23,24}.

This work reports the synthesis and characterization of a new set of magneto-optical glasses based on \text{Tb}^{3+}-containing borogermanate glass compositions. The thermal, structural, morphological, spectroscopic, and optical properties were investigated using differential scanning calorimetry (DSC), X-ray powder diffraction (XRD), high-resolution transmission electron microscopy (HRTEM), and Raman, UV-Vis-NIR, luminescence, and M-Lines spectroscopy methods. The magneto-optical properties were evaluated by Faraday rotation, with Verdet constant (V_B) values measured at different wavelengths in the Vis-NIR range. In addition, a magneto-optical fiber was produced and characterized.

**Results and discussion**

**Thermal, structural, and morphological analysis.** Figure 1 shows the color evolution of the BGB-xTb glasses, as a function of the \text{Tb}^{3+} content. The same color change has been reported for calcium aluminosilicate and borogermanate glasses containing high \text{Tb}^{3+} contents, with the effects being attributed to the \text{Tb}^{3+}-\text{Tb}^{4+} redox process and the conditions of melting$_1,22$.

![Figure 1. Photograph of BGB-xTb glasses with different \text{Tb}_4\text{O}_7 contents.](image)

Figure 2(a) shows the DSC curves for all the BGB-xTb glasses. The characteristic temperatures of glasses, including the glass transition (T_g), onset of crystallization (T_x), and maximum crystallization (T_p), together with the thermal stability parameters (\Delta T = T_x - T_g), were calculated for all the BGB-xTb samples. Table 1 summarizes the values of T_g, T_x, T_p, and \Delta T, together with the density (g cm$^{-3}$) and \text{Tb}^{3+} ions density (ions cm$^{-3}$) values. The \text{Tb}^{3+} ions density was calculated using Equation 1:
\[ N_{Tb^{3+}} \text{ (ions cm}^{-3} \text{)} = \frac{4x\rho N_A}{M} \] (1)

where, \( N_{Tb^{3+}} \) is the density of Tb\(^{3+}\) ions, \( x \) is the mole fraction of Tb\(_4\)O\(_7\), \( N_A \) is the Avogadro constant, and \( M \) is the average molecular weight of the BGB-\(x\)Tb composition.

![Figure 2.](image)

**Figure 2.** (a) DSC curves, (b) \( T_g \) and \( \Delta T \), and (c) optical basicity, as a function of Tb\(_4\)O\(_7\) concentration. The lines in (b) and (c) are just guides for the eyes.

| Sample label | \( T_g \) | \( T_x \) | \( \Delta T \) | \( \rho \text{ (±0.002 g cm}^{-3} \text{)} \) | \( N_{Tb^{3+}} \text{ (10}^{23} \text{ ions cm}^{-3} \text{)} \) |
|--------------|------------|------------|----------------|---------------------------------|---------------------------------|
| BGB-0Tb      | 545        | 740        | 195            | 3.449                           | 0                              |
| BGB-4Tb      | 570        | 766        | 196            | 4.504                           | 20.0                           |
| BGB-6Tb      | 585        | 842        | 257            | 4.766                           | 26.2                           |
| BGB-8Tb      | 605        | 910        | 305            | 5.035                           | 31.1                           |
| BGB-14Tb     | 684        | 814        | 130            | 5.722                           | 39.2                           |
| BGB-16Tb     | 720        | 820        | 100            | 5.984                           | 41.2                           |
| BGB-18Tb     | 703        | 837        | 118            | 6.119                           | 42.0                           |

**Table 1.** Glass transition temperature (\( T_g \)), crystallization onset temperature (\( T_x \)), maximum crystallization temperature (\( T_p \)), thermal stability parameter (\( \Delta T \)), density (\( \rho \)), and Tb\(^{3+}\) ion density values for the BGB-\(x\)Tb glasses.
As can be seen in Figure 2b, the $T_g$ values increased as a function of the Tb$^{3+}$ content, ranging from 545 °C (BGB-4Tb) to 720 °C (BGB-16Tb), followed by a decrease for the most concentrated sample, suggesting the occurrence of structural changes. It has been shown that in borogermanate glasses, RE ions may act as glass modifiers by breaking Ge-O-Ge bonds and inducing the formation of boroxol rings$^{8,25}$. However, for the highest RE content, the structural connectivity was lost, resulting in a decrease of $T_g$. The BGB-$x$Tb glasses presented high $\Delta T$ values, with a maximum of 305 °C for the BGB-8Tb sample, so this sample was the one selected for fiber production.

The optical basicity concept is based on the nature of the chemical bonding, according to Lewis acid-base theory and electronic polarization$^{26,27}$. Duffy$^{26,27}$ proposed an expression (Equation 2) based on optical basicity theory to calculate the average donor power of different constituents of a medium such as a multi-component oxide glass, since $\Lambda_{th}$ is related to the physical and chemical properties of glasses, including their structures and Verdet constants$^{13}$:

$$\Lambda_{th} = \sum x_i A_i$$  \hspace{1cm} (2)

where, $x_i$ is the mole fraction for one of the glass precursors ($i$) and $A_i$ is the theoretical optical basicity value of an individual glass precursor. The intrinsic optical basicities of GeO$_2$, B$_2$O$_3$, Al$_2$O$_3$, Na$_2$O, BaO, and Tb$_2$O$_3$ are 0.600, 0.420, 0.600, 1.15, 1.15, and 0.954, respectively$^{27}$.

Qualitatively, $\Lambda_{th}$ is related to the electron donor power in a glass. In structural terms, the $\Lambda_{th}$ values assist in understanding the increase or decrease of non-bridge oxygen (NBO) (negatively charged) generated by a modifier agent in the glass$^{13}$. According to Liu et al.$^{28}$ and Duffy$^{27}$, a lower value of $\Lambda_{th}$ reflects a lower content of NBO, so lower oxidation numbers of positively charged cations in the glass composition are consequently preferred.

As shown in Figure 2(c), the $\Lambda_{th}$ values increased as a function of the Tb$_4$O$_7$ content. This increase of $\Lambda_{th}$ could be explained by the greater polarizability of the glasses after the addition of Tb$_4$O$_7$, as well as the modifier action of Tb$^{3+}$ ions in the glass network, which contributed to increasing the NBO bonds from the depolymerization of the germanate chains of the glass. Further evidence of NBO bonds in the BGB-$x$Tb glass will be discussed in the Raman spectroscopy section. The $\Lambda_{th}$ values ranged from 0.720 (0Tb glass) to 0.763 (18Tb glass), with increase of Tb$_4$O$_7$. As reported by Yin et al.$^{13}$ and Sontakke et al.$^{29}$, high glass optical basicity is one of the factors contributing to the oxidation of Tb$^{3+}$ to Tb$^{4+}$ during the melting process, responsible for the red shift of the cutoff wavelength. Furthermore, it has been suggested that the addition of high concentrations of Tb$_4$O$_7$ may influence the modifier action of the glassy network constituted by Ge-O-Ge and B-O-B bridging bonds (BO), due to the fact
that the Tb₄O₇ structure contains voluminous polyhedrons larger than those formed by GeO₂ and B₂O₃.

From Table 1, it can be seen that increasing the content of Tb³⁺ led to densification of the matrix, as shown by the higher density values. It should be noted that higher density values are reflected in a higher refractive index, resulting in higher Verdet constants, as will be discussed below.

Figure 3 shows the XRD patterns for the BGB-xTb samples. The diffractograms showed the presence of an amorphous halo and the absence of crystallization peaks, even for the highest Tb₄O₇ content. The halo maximum shifted from 27.5° to 30.5°, while the second halo shifted from 45° to around 50°, corroborating the structural changes induced by the addition of Tb₄O₇, as discussed above.

Figure 3. XRD patterns for the BGB-xTb glasses.

Figure 4(A) shows an HRTEM image of the BGB-18Tb glass, revealing a homogeneous distribution of atoms, with no evidence of clustering at the atomic scale. Fast Fourier transform (FFT) (inset of Figure 4A) confirmed the absence of crystalline spots and the existence of long-range structural order, corroborating the XRD measurements. Figure 4(B) shows a high-angle annular dark-field (HAADF) image of the homogeneous structure of the BGB-18Tb glass (analyzed area) and the corresponding elemental EDS mapping (Ba-K, Tb-L, and O-K). Figure S1 shows the EDS spectrum of the BGB-18Tb glass.
Raman spectroscopy. Raman spectra of all the BGB-xTb glasses are shown in Figure S2(a). The Raman spectrum of the undoped glass (BGB-0Tb) is also plotted to facilitate discussion of the role of Tb$^{3+}$ ions in the glassy network. Raman spectra of the glass formers GeO$_2$ (α-quartz-like) and B$_2$O$_3$ (vitreous) are shown in Figure S2(b).

The Raman spectra showed broad bands typical of glassy structures, assigned to a large distribution of bonds and angles, as well as several overlapping vibrational modes of the glass components. For these reasons, it was necessary to identify the contributions of the individual vibrational modes by deconvolution, involving the fitting of Gaussian peaks in different frequency regions of the spectra. Such Gaussian deconvolution has been described in previous spectroscopic studies of germanate, borate, and borogermanate glasses$^{8,20,25,30-36}$.

Raman spectra of the BGB-xTb glasses at low (~130-700 cm$^{-1}$), medium (~650-1050 cm$^{-1}$), and high (1050-1800 cm$^{-1}$) frequencies are shown in Figure 5(a-c). Figure 5(d-o) shows the deconvolution at low, medium, and high frequencies for the BGB-xTb glasses ($x = 0, 4, 8, \text{and 18 mol} \% \text{ of Tb}_4\text{O}_7$). It can be seen that the addition of Tb$_4$O$_7$ caused structural changes in the BGB glass network. The main vibrational modes assigned from the Raman spectra for the BGB-xTb glasses are summarized in Table 2.
Figure 5. Normalized Raman spectra for the BGB-\(x\)Tb glasses in (a) low (~130-700 cm\(^{-1}\)), (b) medium (~650-1050 cm\(^{-1}\)), and (c) high (1050-1700 cm\(^{-1}\)) frequency regions. Deconvolution of the Raman spectra for the 0, 4, 8, and 18Tb glasses in the low (d–g), medium (h–k), and high (l–o) frequency regions.
Peaks | Frequencies (cm\(^{-1}\)) | Vibrational modes | References
--- | --- | --- | ---
1 and 2 | 220 and 305 | Bending modes of Ge-O in the glassy network | 31-33
3 | 340-410 | Vibration of Ge-O\(^-\) (NBO) corresponding to the Q\(^1\) species | 31, 33, 34, 37
4 | 470 | Symmetrical stretching vibrations of Ge-O-Ge bonds in 3-membered GeO\(_4\) rings | 35, 37
5 | 520 | Vibrations of Ge-O-Ge bonds in three-membered GeO\(_4\) | 35-37
6 | 574-598 | Symmetrical vibrations of Ge-O-Ge | 35-37
7 | 747 | Symmetrical stretching vibrations of metaborate chains | 32, 34, 37
8 | 740-777 | Vibrations of borate rings (di-triborate rings) | 32, 34, 37
9 | 810-820 | Symmetrical stretching vibrations of Ge-O\(^-\) (NBO) in Q\(^2\) species | 36, 38
10 | 790-830 | Symmetrical stretching vibrations of Ge-O\(^-\) (NBO) in Q\(^3\) species | 36, 38
11 | 907-930 | Vibrational mode of diborate groups | 36
12 | 1200 | Diborates | 36
13 | 1337 | BO\(_{3/2}\) | 36
14 | 1427 | BO\(_{3/2\text{ring}}\) | 36
15 | 1495 | B-O\(^-\) | 36

Table 2. Assignments of the main vibrational modes for the BGB-\(x\)Tb glasses.

Figure 5(d) shows the peak fitting for the undoped BGB glass. In this case, six Gaussian peaks were fitted at low frequencies: 220 (peak 1), 305 (peak 2), 350 (peak 3), 470 (peak 4), 518 (peak 5), and 561 cm\(^{-1}\) (peak 6). In the region below 400 cm\(^{-1}\), peaks 1 and 2 could be attributed to bending modes of Ge-O-Ge in the glassy network\(^{32,33}\). Peak 3 could be assigned to the vibration of Ge-O\(^-\) (Q\(^1\) species)\(^{31,33,34,37}\). Peak 4 was assigned to symmetrical stretching
vibrations of Ge-O-Ge bonds in 3-membered GeO$_4$ rings$^{35,37}$. Between 500 and 600 cm$^{-1}$, peaks 5 and 6 could be attributed to vibrations of Ge-O-Ge bonds in three-membered GeO$_4$ and symmetrical vibrations of Ge-O-Ge$^{35-37}$. The presence of only Ge$^{4+}$ in borogermanate glasses was recently elucidated using Ge K-edge EXAFS and XANES measurements$^8,20$.

Two main features could be observed after addition of terbium oxide: (I) the intensity of the broad band between 130 and 400 cm$^{-1}$ increased, and (II) the intensity of the broad band between 500 and 650 cm$^{-1}$ was strongly attenuated. These behaviors could be explained by the gradual increase of Ge-O$^-$ non-bridge bonds (NBO), due to depolymerization of the BGB glass network after addition of Tb$^{3+}$ ions. In region I, according to Kamitsos et al.$^{33}$ and Nakamoto$^{37}$, the appearance of vibrational modes at low frequencies (200-400 cm$^{-1}$) could be assigned to the bending modes of Q$^2$ and Q$^1$ species derived from GeO$_4$ units, as detailed in Figure 5(d-g). In region II, depolymerization increased the NBO number, consequently decreasing the average distribution of Ge-O-Ge bridges.

The deconvolution of the middle region is shown in Figure 5(h-k). Deconvolution of the broad band centered at around 828 cm$^{-1}$ resulted in the fitting of five peaks centered at around 753, 778, 815, 828, and 908 cm$^{-1}$. The first two (peaks 7 and 8) were assigned to the symmetrical stretching vibrations of metaborate chains and borate rings (di-triborate rings), respectively$^{32,34,37}$. Previous investigations of germanate and borogermanate glasses using Raman spectroscopy found that the region between 800 and 900 cm$^{-1}$ was dominated by vibrational modes of Q$^2$ and Q$^3$ units derived from the breakdown of tetrahedral [GeO$_4$] units$^{31,32,35-37}$. Peaks 9 (815 cm$^{-1}$) and 10 (828 cm$^{-1}$) could be attributed to symmetrical stretching vibrations of Ge-O$^-$ in Q$^2$ and Q$^3$ species, respectively$^{36,38}$. In addition, peak 11 (~908 cm$^{-1}$) was assigned to diborate groups$^{36}$.

As shown in Figure 5(b), the addition of Tb$_4$O$_7$ shifted the broad band centered at 828 cm$^{-1}$ (BGB-0Tb glass) to 792 cm$^{-1}$ (BGB-18Tb glass), while the shoulder at 909 cm$^{-1}$ in the BGB-0Tb spectrum was shifted to 931 cm$^{-1}$. Koroleva et al.$^{36}$ used Raman spectroscopy to evaluate the individual contributions of the vibrational modes of B$_2$O$_3$ and GeO$_2$ in borogermanate glasses. Based on the work of Koroleva et al.$^{36}$ and Kamitsos et al.$^{33}$, the band observed between 900 and 940 cm$^{-1}$ (peak 11) in the Raman spectra of the borogermanate glasses could be assigned to the vibration of diborate groups.

At higher frequencies (above 1050 cm$^{-1}$), there was a predominance of vibrations of borate groups (Figure 5(c)). The Raman spectrum for the BGB-0Tb glass presented a band at 1200 cm$^{-1}$ (peak 12), assigned to diborate groups, and a broad band at around 1427 cm$^{-1}$ with overlapping peaks assigned to asymmetric stretching of B-O bonds of BO$_3$/2 units (peak 13, at
1337 cm⁻¹, stretching vibration of BO₃/2ring (peak 14, at 1427 cm⁻¹), and vibrations related to non-bridging oxygen atoms of B-O' bonds (peak 15, at 1495 cm⁻¹)³⁶.

The Raman analysis revealed an interesting feature of borogermanate glasses that should be considered in the search for glasses presenting extremely high Verdet constants. \( V_B \) was shown to be dependent on the Tb³⁺ ions and increased as a function of the rare earth content. In order to introduce high contents of rare earths into glasses, it is necessary to provide a favorable chemical environment, since rare earths need high coordination number of oxygen atoms to be stabilized and to avoid further precipitation. From comparison of the structures of the glasses studied in this work with other compositions presented in the literature, it could be inferred that increase in the number of NBO can assist in the stabilization of rare earths³⁹. For compositions containing lower quantities of NBO, the amounts of rare earths were lower than for those with higher NBO, which was mainly characterized by the intense bands at ~300 and 820 cm⁻¹ (Ge-O') and above 1050 cm⁻¹ (B-O'). Hence, the use of adequate contents of modifiers such as BaO is essential for obtaining higher \( V_B \) in borogermanate glasses.

**Optical analysis.** Figure 6(a) shows the absorption spectra of the BGB-xTb glasses in the region from 250 to 800 nm. The absorption bands at 318, 340, 350, 358, 370, 378, and 485 nm were assigned to the Tb³⁺ 4f-4f transitions from the \( ^7F_6 \) ground state to the excited states \( (^7D_0, ^5H_7), (^5G_2, ^5L_6), ^5L_9, ^5G_5, ^5L_{10}, (^5D_3, ^5G_6), \) and \( ^5D_4, \) respectively⁴⁰.
Figure 6. (a) UV-Vis-NIR optical absorption, (b) transmission spectra, (c) refractive indices as a function of Tb$_4$O$_7$ content, at different wavelengths, and (d) refractive indices for BGB-$x$Tb glasses ($0 \leq x \leq 18$), as a function of wavelength.
As shown in Figure 6(a), the UV cutoff for the undoped glass was at around 300 nm. The red shift to around 600 nm (BGB-18Tb), observed after addition of Tb₄O₇, was the result of the intense absorption of the Tb³⁺ transitions. However, the main origin of the red shift could be ascribed to the oxidation of Tb³⁺ to Tb⁴⁺, characterized by the change of color from colorless, passing through pale yellow, and finally to dark brown, as the Tb³⁺ content increased (see Figure 1)⁴¹.

Figure 6(b) shows the transmission window for the BGB-xTb glasses, recorded from UV to NIR. In the visible region, there were the absorption bands assigned to the 4f electronic transitions of Tb³⁺ ions. In the NIR region, at 1.84, 1.93, 2.06, and 2.46 μm, there were the 4f-4f transitions of Tb³⁺ ions from the ⁷F₆ ground state to the ⁷F₀, ⁷F₁, ⁷F₂, and ⁷F₃ excited states, respectively²⁰,⁴¹. It should be highlighted that the BGB-xTb glasses containing up to 8 mol% Tb₄O₇ presented optical windows from 0.5 μm up to 1.60 μm.

Figure 6(c) shows the refractive indices (n) for the BGB-xTb samples, in the visible and near-infrared regions, as a function of Tb₄O₇ content. It can be seen that increase of the Tb₄O₇ concentration resulted in a higher value of n, mainly due to the high polarizability of the Tb³⁺ ions. The maximum n obtained was 1.8457 at 532 nm, for the BGB-18Tb glass. Figure 6(d) shows the refractive indices as a function of wavelength. The curve profiles showed that decrease of n was associated with increase of the wavelength, indicative of chromatic dispersion⁴².

**Luminescence analysis.** Figure 7(a-b) shows the photoexcitation (PLE) and luminescence (PL) spectra of Tb³⁺ in the BGB-xTb glasses at room temperature. Figure 7(a) shows the PLE spectrum of the BGB-4Tb glass excited at 545 nm. Overlapping was observed of PLE bands in the UV-Vis region at 483, 375, 370, 357, 350, 339, 325, 316, 301, and 284 nm, corresponding to 4f⁸ → 4f⁸ electronic transitions from the ⁷F₆ ground state to the labeled excited states⁴³. The most intense band at 375 nm, assigned to the ⁷F₆ → ⁵D₃ transition, was used as the excitation wavelength for acquisition of the emission spectra shown in Figure 7(b).
Figure 7. (a) PLE spectrum of the BGB-4Tb glass and (b) PL spectra of the BGB-xTb glasses at room temperature. Inset photograph: BGB-4Tb sample under excitation at 375 nm. Inset: PL spectra of the BGB-xTb glasses (x = 14, 16, and 18 mol% Tb\textsubscript{4}O\textsubscript{7}) in the region from 530 to 560 nm.

Four emission bands at 487, 541, 582, and 620 nm were assigned to the transitions from $^5\text{D}_4$ to $^7\text{F}_j$ ($j = 6,5,4,3$) multiplet\textsuperscript{44}. Comparison of all the PL bands of the Tb\textsuperscript{3+} ions in the BGB glasses showed the same spectral profile for all the samples, although the intensities of the PL bands differed, since strong quenching in BGB glasses is observed with increase of the Tb\textsubscript{4}O\textsubscript{7} concentration. This fluorescence quenching is due to greater interaction between the RE ions present at higher concentrations, with shorter distances between neighboring ions (Tb\textsuperscript{3+}-Tb\textsuperscript{3+}) in the bulk glass\textsuperscript{45}. The inset in Figure 7(b) highlights the low intensity emission assigned to the electronic transition at 541 nm for the BGB-xTb glasses (x = 14, 16, and 18 mol% Tb\textsubscript{4}O\textsubscript{7}) in the range between 530 and 560 nm.

Figure S3 shows the normalized luminescence decay curves for the $^5\text{D}_4 \rightarrow ^7\text{F}_7$ emission of Tb\textsuperscript{3+} ions for the BGB glasses containing $x = 4, 6, 8, \text{ and } 14$ mol% Tb\textsubscript{4}O\textsubscript{7} obtained by monitoring of the green emission at 545 nm, with excitation at 375 nm. The decay times for the BGB-xTb ($x = 16$ and 18) glasses are not shown, due to the strong quenching. The decay
curves presented a single exponential profile, described by \( I(t) = I_0 \exp(-t/\tau) \), where \( \tau \) (in ms) is the lifetime. The graph inserted in Figure S3(c) shows the fluorescence decay time as a function of \( \text{Tb}_4\text{O}_7 \) concentration, where \( \tau \) decreased with increase of the \( \text{Tb}^{3+} \) content from 1.38 ms (\( x = 4\text{Tb} \)) to 0.175 ms (\( x = 14\text{Tb} \)).

**Magneto-optical properties and Verdet constant** \((V_B)\). In this work, BGB glasses containing high concentrations of \( \text{Tb}^{3+} \) ions showed accentuated Faraday rotation effects in the visible and NIR regions. The theory underlying the Faraday effect in glasses is based on the Zeeman effect when the material is submitted to a magnetic field\(^9,11\). The magnitude of the Faraday effect in a magneto-optical material is evaluated by calculation of the Verdet constant \((V_B)\)\(^9\).

Figure 8(a) shows the set of transparent BGB-\(x\)Tb bulk glasses and the magnetic attraction of the BGB-18Tb glass using a commercial neodymium-based magnet (N42 grade). This interesting attraction phenomenon is a qualitative way to demonstrate the paramagnetic properties of BGB-\(x\)Tb bulk glasses. All the glasses studied here could be lifted using the Nd magnet. A video showing the attraction effect is provided with the online version of the manuscript.

Figure 8(b-c) shows the \( V_B \) values as a function of the concentration of \( \text{Tb}_4\text{O}_7 \) (in mol\%) and the \( \text{Tb}^{3+} \) ion density (in \( 10^{21} \) ions cm\(^{-3} \)) for all the glasses, at different wavelengths. The increase of the \( V_B \) values with the \( \text{Tb}_4\text{O}_7 \) content is shown in Figure 8(b). The \( V_B \) values obtained were negative, indicating right-handed rotation of the polarized light, characteristic of paramagnetic materials.
Figure 8. (a) Photographs of the BGB-xTb glasses and the magnetic attraction of the BGB-18Tb glass using a commercial neodymium magnet. Plots of $V_B$ as a function of (b) Tb$_4$O$_7$ content (mol%), (c) Tb$^{3+}$ ions density (g cm$^{-3}$), and (d) wavelength.

In studies of the MO properties of RE-doped glasses, the $V_B$ values are generally expressed as a function of the RE ion density ($N_{RE\ ion}$). In this work, the Tb$^{3+}$ ion densities ($N_{Tb^{3+}}$) for all glasses were calculated using Equation (1) and are shown in Table 1.

Progressive increase of the Tb$^{3+}$ content led to improvement of the magneto-optical properties of the glasses (Figure 8(c)), as confirmed by increase of the $V_B$ values. At 500 nm, $V_B$ for the BGB-8Tb glass was -111.5 rad T$^{-1}$ m$^{-1}$, while the $V_B$ values at 650 nm for the BGB-4Tb and BGB-18Tb glasses were -43.0 and -128.0 rad T$^{-1}$ m$^{-1}$, respectively. At 650 nm, the BGB-18Tb glass had the highest $V_B$ value among all the glasses studied in this work. The observed values were consistent with those reported in the literature for other borogermanate glasses$^{1,22}$. In addition, comparison of the $V_B$ values for the BGB-18Tb glass and the TGG
reference, at 650 nm, showed that the $V_B$ of the glass was only 2.3% higher than the value for TGG ($V_B = -125 \text{ rad T}^{-1} \text{ m}^{-1}$\textsuperscript{19}).

The MO effect of glasses containing high Tb\textsuperscript{3+} contents is due to the unfilled 4f electron layer of Tb atoms, since the unpaired 4f electrons generate random magnetic moments, consequently inducing a strong paramagnetic effect. In other words, for Tb\textsuperscript{3+}, the high magnetic moment and the paramagnetic effect are produced from 4f $\rightarrow$ 4f\textsuperscript{n-1} 5d energy level transitions\textsuperscript{11,46}. In general terms, the Verdet constant for MO glass can be described by the sum of the contributions of paramagnetic and diamagnetic components, according to Equation (3)\textsuperscript{13}:

$$V_B = V_{\text{paramag}} + V_{\text{diamag}} \quad (3)$$

where, $V_{\text{paramag}}$ and $V_{\text{diamag}}$ are the Verdet constants for the paramagnetic and diamagnetic contributions. Therefore, when $V_{\text{paramag}}$ is higher than $V_{\text{diamag}}$, the MO glass is predominantly paramagnetic. As discussed before, a useful way to increase the $V_{\text{paramag}}$ component in a MO glass is by adding paramagnetic species such as Tb\textsuperscript{3+}, Dy\textsuperscript{3+}, or Mn\textsuperscript{2+} ions\textsuperscript{1,7,47}. The proportional inverse relationship between $V_{\text{paramag}}$ and wavelength can be expressed as shown in Equation (4)\textsuperscript{13}:

$$V_{\text{paramag}}(\lambda) = \frac{A}{\lambda^2 - \lambda_t^2} \quad (4)$$

where, $A$, $\lambda$, and $\lambda_t$ are approximation parameters and are given as the incident light and the effective transition wavelengths, respectively\textsuperscript{13}. Figure 8(d) shows the inverse relation between $V_B$ and wavelength for all the BGB-xTb samples, as described by Equation 4.

The Figure 8(d) inset shows the relationship between $I/V_B$ and $\lambda^2$ for the BGB-18Tb glass data. The value of $\lambda_t$ was obtained as the intersection of the straight line on the x-axis ($\lambda^2$), obtained from linear fitting of $I/V_B$ vs. $\lambda^2$. In this case, the value of the effective transition wavelength ($\lambda_t$) for the BGB-18Tb glass was 228 nm, which was close to the 4f\textsuperscript{8} $\leftrightarrow$ 4f\textsuperscript{7} 5d electron energy level transition of Tb\textsuperscript{3+}, specifically the $^7F_6$-$^7D_5$ level transition between 220 and 250 nm\textsuperscript{48}. The $\lambda_t$ value of 228 nm for the BGB-18Tb glass was similar to values reported for other glass systems such as fluorophosphate (~217 nm)\textsuperscript{49}, borogermanate (225-300 nm)\textsuperscript{1}, sodium borate (~220 nm)\textsuperscript{50}, Tb\textsuperscript{3+}-doped phosphate (~250 nm)\textsuperscript{51}, aluminoborate (~250 nm)\textsuperscript{52}, and borosilicate (~259-280 nm)\textsuperscript{53}.
The main wavelengths for applications of MO glasses are in the infrared range, between 1.05 and 1.33 µm\textsuperscript{54}. Figure 8(d) shows the $V_B$ values obtained for all the glasses at 1.03, 1.33, and 1.55 µm. It should be highlighted that the maximum $V_B$ value at 1550 nm (in the telecommunications range) was -17.6 rad T\textsuperscript{-1} m\textsuperscript{-1}, which was 37-fold higher than the $V_B$ of silica glass (~0.471 rad T\textsuperscript{-1} m\textsuperscript{-1})\textsuperscript{55}.

For practical purposes, the absorption of the glass in the spectral region employed should be minimized. As observed in this work, the optical window diminishes as a function of the terbium content, mainly due to the oxidation of Tb$^{3+}$ to Tb$^{4+}$, which occurs at high temperature. However, this problem can be mitigated by the addition of reducing agents such as Ce$_2$O$_3$, as shown in Figure S4, which allow broadening of the optical window in the visible range. As can be seen, the addition of 0.5 mol\% Ce$_2$O$_3$ was sufficient to maintain the reduced conditions necessary to avoid oxidation of Tb$^{3+}$ to Tb$^{4+}$, without significantly affecting other thermal and structural properties. With this approach, it was possible to shift the absorption band from 0.75 to 0.55 µm and obtain a glass that was light yellow in color, rather than dark brown, as shown in the inset in Figure S4.

**Fabrication of magneto-optical glass fiber.** Figure 9(a-b) shows photographs of the polished glass preform and the optical fiber obtained by applying the drawing process to the BGB-8Tb glass. Among all the BGB glasses analyzed, the BGB-8Tb glass presented the highest $\Delta T$, so for this reason it was selected for production of the magneto-optical fiber. The BGB-8Tb fiber was coated with poly(methyl methacrylate) (PMMA) and the length of the fiber obtained was around 50 m (Figure 9(b)).
Figure 9. (a) Glass preform, (b) MO fiber based on the BGB-8Tb composition, (c) SEM cross-section image of the BGB-8Tb fiber, (d) glass preform after the drawing process, and (e) optical microscopy image of the surface of the fiber.

Figure 9(c) shows an SEM cross-section image of the optical fiber with diameter of around 237 μm. The refractive index of the BGB-8Tb fiber was 1.7514, measured at 532 nm. This value was the same as obtained for the corresponding bulk sample.

Figure 9(d-e) shows photographs of the preform after the drawing process and the surface of the optical fiber, respectively. In neither case was there any evidence of crystallization on the surface after the drawing process.

**Magneto-optical and optical fiber characterizations.** Figure 10(a) shows the $V_B$ values for the BGB-8Tb fiber according to wavelength. The $V_B$ values obtained in the visible range at 500 and 650 nm were -110.2 and 58.8 rad T$^{-1}$ m$^{-1}$, respectively. In the NIR range, the $V_B$ values were -32.2, -22.8, -15.2, and -9.5 rad T$^{-1}$ m$^{-1}$ at 880, 1050, 1330, and 1550 nm, respectively.

Comparison with $V_B$ values at 650-660 nm reported in the literature showed that the $V_B$ values for the BGB-8Tb fiber were higher than for Eu$^{3+}$-doped silica$^{11}$ (-4.564 rad T$^{-1}$ m$^{-1}$), Er$^{3+}$-doped silica (EDF)$^{11}$ (-3.379 rad T$^{-1}$ m$^{-1}$), Ho$^{3+}$-doped silica$^{21}$ (-23.6 rad T$^{-1}$ m$^{-1}$), and Tb$^{3+}$-doped borogermanate$^{20}$ (-23.6 rad T$^{-1}$ m$^{-1}$). However, at 1053 nm, $V_B$ obtained here was lower than for silicate fibers containing 56 and 65 wt% Tb$^{3+}$ ions, for which the values were -24 and -32 rad T$^{-1}$ m$^{-1}$, respectively$^{17,24}$. It should be highlighted that the $V_B$ values for the BGB-8Tb fiber
at 1050 and 1550 nm (-22.8 and -9.5 rad T\(^{-1}\) m\(^{-1}\), respectively) were nineteen and sixteen times higher than for a single-mode optical fiber (SMF) (V\(_B\) ~0.589 rad T\(^{-1}\) m\(^{-1}\) at 1550 nm\(^{17,24}\)).

Figure 10. (a) Variation of the Verdet constant as a function of wavelength and (b) attenuation spectrum of the BGB-8Tb fiber determined using the cut-back method, with a final length of 0.21 cm.

Figure 10(b) shows the attenuation spectrum of the BGB-8Tb fiber, revealing two main optical losses in the ranges 350-500 nm and 1400-1750 nm. As observed in the transmission spectra for the BGB-\(x\)Tb bulk glasses (Figure 6b), there were intrinsic absorptions in UV-Vis-NIR regions, attributed to the Tb\(^{3+}\) ions. Using the cut-back method (from 1.92 m to 0.21 cm fiber length), the minimum attenuation of 6.4 dB m\(^{-1}\) was obtained at around 880 nm (Figure 10(b)). The main sources of fiber attenuation include the glass preform preparation process, traces of impurities, water absorption, glass striae, and fiber imperfections.

Among the optical fibers reported in the literature, pure silica fibers are known to provide high performance, due to low attenuation in the NIR region\(^{56}\). On the other hand, silica fibers have very low V\(_B\) values in the NIR region\(^{11}\). For example, V\(_B\) of ~2.05 rad T\(^{-1}\) m\(^{-1}\) was found for an SMF at 830 nm\(^{57}\). In this work, the BGB-8Tb fiber presented V\(_B\) of -32.2 rad T\(^{-1}\)
m$^{-1}$ at 880 nm, which was around 15-fold higher than obtained for the SMF$^{57}$. In magneto-optical terms, the BGB-8Tb fiber has good potential for application in the so-called “first optical window” at around 820-900 nm, given its high V$_B$ value at 880 nm$^{58}$.

**Conclusions**

This work reports the synthesis of transparent Tb$^{3+}$-borogermanate MO glasses using the traditional melt-quenching method. The thermal, structural, morphological, spectroscopic, optical, and magnetic-optical properties of the glasses were investigated. Structural changes in the glass network, following the addition of Tb$_4$O$_7$, were confirmed by Raman spectra of the BGB-xTb glasses, showing the presence of vibrations assigned to non-bridging oxygen bonds, such as Ge-O$^-$ in Q$^2$ and Q$^3$ species, and B-O$. The morphological analyses showed that at high Tb$^{3+}$ content, the BGB-xTb system was free of nanocrystals. The absence of crystals and high thermal stability of the glass containing 8 mol% of Tb$_4$O$_7$ (305 °C) allowed the production of an MO fiber. The magnitude of the Faraday effect in the BGB-xTb glasses was evaluated from the V$_B$ values in the visible and NIR regions. Here, it should be emphasized that the V$_B$ values for the BGB-xTb glasses were investigated in the NIR region, between 880 and 1550 nm. An important finding was that the maximum V$_B$ value at 1550 nm was -17.6 rad T$^{-1}$ m$^{-1}$, which was 37 times higher than for silica glasses. The maximum Verdet constant value for the BGB-18Tb glass at 650 nm was -128 rad T$^{-1}$ m$^{-1}$. For the BGB-8Tb optical fiber, V$_B$ at 1550 nm (telecommunications range) was -9.5 rad T$^{-1}$ m$^{-1}$, which was 16 times higher than V$_B$ for silica glass. The lowest optical loss of 10 dB m$^{-1}$ and V$_B$ of -32.2 rad T$^{-1}$ m$^{-1}$ were measured at 880 nm. In summary, the BGB-xTb system provides a set of MO glasses with potential to produce Faraday rotator fibers.

**Methods**

**Synthesis.** Tb$^{3+}$-doped borogermanate glasses were prepared by the conventional melt-quenching method, using chemical-grade germanium oxide GeO$_2$ (Sigma-Aldrich), boric acid (H$_3$BO$_3$, Sigma-Aldrich), aluminum oxide (Al$_2$O$_3$, Sigma-Aldrich), sodium carbonate (Na$_2$CO$_3$, Sigma-Aldrich), barium carbonate (BaCO$_3$, Sigma-Aldrich), and terbium oxide (Tb$_4$O$_7$, Sigma-Aldrich).

The chemicals were stoichiometrically weighed to yield 10 g of a glass with molar composition of (100-x)(41GeO$_2$-25B$_2$O$_3$-4Al$_2$O$_3$-10Na$_2$O-20BaO) – xTb$_4$O$_7$ (BGB-xTb),
where $x = 0, 4, 6, 8, 14, 16, \text{and} 18 \text{ mol\%}$. The samples were labeled as BGB-$x$Tb. All the compositions are summarized in Table 1.

In the first step, vitreous boron oxide was obtained by thermal decomposition of $\text{H}_3\text{BO}_3$ at 500 °C for 30 min in a resistive furnace. The glass components were ground to fine powder and homogenized in an agate mortar. Batches were loaded into a platinum crucible and melted at between 1350 and 1500 °C (depending on the $\text{Tb}_4\text{O}_7$ content), for 2 h, under atmospheric conditions. The melt was cooled in a preheated stainless steel mold at 30 °C, below the glass transition temperature ($T_g$), and then annealed at the same temperature for 3 h, to minimize its mechanical stress, followed by slowly cooling to room temperature during 12 h. Pieces with thickness of 3 mm were obtained. As a final step, the samples were polished using silicon carbide (SiC) polishing papers, prior to the optical characterizations.

The glass preform based on the composition 92(41GeO$_2$-25B$_2$O$_3$-4Al$_2$O$_3$-10Na$_2$O-20BaO)-8Tb$_4$O$_7$ (BGB-8Tb) was selected for use in the fiber drawing process, because it showed the highest $\Delta T$ value (305 °C), among the set of glasses analyzed. A glass rod was prepared by melt-quenching, using a 30 g batch of glass. The batch was melted in a platinum crucible tube, at 1450 °C for 1 h, under an atmosphere of N$_2$ at a flow rate of 30 mL min$^{-1}$, in an induction furnace.

The cylindrical stainless steel mold was pre-heated at 555 °C (50 °C below $T_g$) for 2 h before the melt-quenching process, in order to ensure an even temperature. The dimensions of the mold were 10 cm long and 10 mm diameter. The rod preform was annealed for 6 h at 555 °C and cooled at a rate of 0.5 °C min$^{-1}$, requiring 17.5 h to reach room temperature. To minimize the structural stress of the BGB-8Tb preform, a second annealing process was performed under the same conditions used previously. Glass preforms containing high concentrations of RE oxides generally present high structural stress, requiring a long annealing time and a slow cooling rate. After the cooling process, the preform was polished in several steps using SiC papers (600 to 1200 grit).

In the final step, the preform was mounted into the drawing tower and the fiber drawing process was started at 720 °C ($T_g + 115$ °C). During the drawing process, the BGB-8Tb fiber was coated with a low-index UV-cured poly(methyl methacrylate) (PMMA) polymer, in order to protect the magneto-optical fiber and improve its mechanical properties.

**Measurements and characterizations.** Differential scanning calorimetry (DSC) measurements of the BGB-$x$Tb glasses were performed using a Netzsch DSC Pegasus 404F3 apparatus. For this, the glass sample (10 mg) was placed in a platinum crucible and heated from
25 to 1000 °C, at a rate of 10 °C min\(^{-1}\), under an atmosphere of nitrogen (20 mL min\(^{-1}\)). The maximum errors were ±2 °C for \(T_g\) and \(T_x\), and ±4 °C for \(\Delta T\).

Powder X-ray diffraction measurements were carried out with a Panalytical Aries benchtop diffractometer operating with a Cu K\(\alpha\) radiation source. Scanning was performed in the 20 range from 10° to 80°, with step size of 0.01° and step time of 2 s.

Raman spectra were recorded at room temperature, in the frequency range from 100 to 1800 cm\(^{-1}\), using a Renishaw inVia Micro-Raman spectrometer equipped with a 633 nm laser delivering 17 mW, coupled with a Leica DM2700 microscope.

HRTEM images and SAED patterns for the BGB-18Tb glass were obtained using an FEI Tecnai G2 F20 (200 kV) transmission electron microscope equipped with a field emission gun, coupled with an energy dispersive spectroscopy (EDS) microanalysis system. For the analysis, the BGB-18Tb glass was finely powdered, suspended in ethanol, and deposited onto a copper grid.

Density measurements were performed with a Mettler Toledo Excellence XS densimeter. The measurement precision was ±0.002 g cm\(^{-3}\).

Optical absorption and transmission spectra of the BGB-\(x\)Tb glasses were obtained using a Varian Cary 500 dual-beam UV-Vis-NIR spectrophotometer, in the ranges from 200 to 800 nm and from 0.25 to 3 \(\mu\)m, respectively. Linear refractive indexes for the BGB samples were determined at 532, 633, 972, 1038, and 1538 nm by the prism coupling technique, using a Metricon 2010 M-Lines instrument, with precision of ±0.0001.

Excitation, emission, and photoluminescence decay curves were obtained using a Fluorolog near-infrared photomultiplier tube system (NIR-PMT) (Horiba Jobin Yvon) equipped with a xenon lamp (200-900 nm). The PL measurements were performed with bulk samples, at room temperature.

**Faraday rotation measurements.** Faraday rotation values of the BGB-\(x\)Tb glasses were obtained at room temperature, using a neodymium magnet with a total magnetic field (\(B\)) of 0.46 T. For the Faraday rotation angle (\(\theta\)), a standardized sample length (\(l\)) of 1.9 cm was used. The faces of all the samples were polished to obtain flat surfaces. The Faraday rotation angles were measured at 500, 650, 880, 1030, 1308, and 1550 nm, using a SuperK COMPACT supercontinuum laser (NKT Photonics) with spectral range from 450 to 2400 nm, power of 100 mW, and operating temperature range of 15-30 °C.

The laser beam was focused on the BGB-\(x\)Tb sample and the polarized light transmitted through the glass was measured using a graduated polarizer. The output beam was detected at
500, 650, 880, and 1050 nm, using a PM100D Handheld Optical Power and Energy Meter (Thorlabs), and at 1330 and 1550 nm, using a PDA015C InGaAs Fixed Gain Amplified Detector (Thorlabs) connected to a Model 2512 100 MHz 1 GSa/s Handheld Digital Storage Oscilloscope (BK Precision).

Similarly, Faraday rotation angle measurements for the BGB-8Tb fiber were performed at 500, 650, 880, 1050, 1330, and 1550 nm. The input and output fibers were cleaved using a 24X0-RCL cleaving machine and the optical path length \( l \) was 2 cm. The fiber was inserted in a holder and a 40x objective lens was used to focus the laser onto the fiber section. The Faraday rotation angles were measured in triplicate, using a polarizer with precision of ±2°. The Verdet constant values \( V_B \) (rad T\(^{-1}\) m\(^{-1}\)) were obtained from the Faraday rotation (Equation 5).

\[
V_B = \frac{\theta}{l} \tag{5}
\]

**Optical fiber characterization.** The cut-back fiber loss method was used to measure the optical attenuation of the BGB-8Tb fiber in the range from 350 to 1750 nm. The attenuation spectra were acquired using an optical spectrum analyzer (OSA) (Model AQ-6315A, Yokogawa) with wavelength resolution of 5 nm. To obtain flat surfaces, the input and output of the BGB-8Tb fiber were cleaved using a 24X0-RCL cleaving machine, after which the fiber was clamped into two SubMiniature version A (SMA) adaptors. For broadband measurement, the input fiber was clamped at the tungsten-halogen lamp housing and the output was connected to an OSA instrument. The cutback measurements were performed from the initial fiber length of 1.92 m to a final length of 21.8 cm. The output fiber was cut into different lengths using the cleaving machine and the output power was measured for each length, in order to obtain more accurate transmission losses data.

**Data availability**
All data regarding the work presented here are available upon reasonable request to the corresponding authors.
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**Author Contributions**
D.F.F. wrote the paper and synthesized the glass samples and the optical fiber and carried out the DSC, XRD, Raman, UV-Vis, M-Lines, Photoluminescence, Attenuation and Magneto-optical measurements. Y.L. participated in the synthesis of the glass samples and the PL measurements. W.C. participated in the SEM and magneto-optical measurements. S.M. was responsible for the fiber drawing process. C.R.M.A. has carried out the morphological characterization (HRTEM). S.M. participated in the review of the manuscript and contributed to the discussion of data. Y.M. supervised the preparation and characterization of the glass samples and optical fiber and contributed to the discussion of data. M.N. is the supervisor of the project, participated in the writing of the manuscript and contributed to the discussion of data. All authors reviewed the manuscript.

**Competing interests**
The authors declare no competing interests.

**Additional information**
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