A General Computational Treatment of Comparatives
for Natural Language Question Answering

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Abstract

We discuss the techniques we have developed and implemented for the cross-categorial treatment of comparatives in TELI, a natural language question-answering system that's transportable among both application domains and types of backend retrieval systems. For purposes of illustration, we shall consider the example sentences "List the cars at least 20 inches more than twice as long as the Century is wide" and "Have any US companies made at least 3 more large cars than Buick?" Issues to be considered include comparative inflections, left recursion and other forms of nesting, extraposition of comparative complements, ellipsis, the wh element "how", and the translation of normalized parse trees into logical form.

1. Introduction

We shall describe a general treatment of comparatives that has been implemented in the context of TELI, a question-answering system which is transportable among both domains of discourse and different types of backend retrieval systems. Comparatives are important because of the dramatic increase in expressive power they allow; they are interesting at least because of the variety of issues (from morphology on up) one must deal with in order to provide for them.

1.1 Goals

In seeking to provide TELI with general capabilities for comparatives, our primary goals have been to formulate cross-categorial techniques that treat the comparativizations of different syntactic elements (e.g. adjectives, quantifiers, and measure nouns) with the same mechanisms; to allow comparatives to be composed with themselves (e.g. "at least 3 more than 3 times as many") and with other syntactic features (e.g. wh elements); to be faithful to what is known from work in theoretical linguistics; we draw from Bresnan (1973), Cushing (1982), Dik (1980), Jackendoff (1977), Sells (1985), and Winograd (1983); to account for as many of the specific cases of comparatives found in the literature of implemented NL processors as possible.

1.2 Achievements

Letting <X> denote a grammatical category to be comparativized, we begin by providing for comparativized structures C{<X>} of the form

\[
C\{<X>\} \rightarrow (\langle Qual\rangle) CC\{<X>\} \langle Comp\rangle
\]

\[
\langle Qual\rangle \rightarrow \text{at most} \mid \text{at least} \mid \text{no} \mid \text{exactly} \mid \text{precisely} \mid \text{just} \mid \text{only}
\]

\[
CC\{<X>\} \rightarrow (CC\{<X>\}) \langle Measure\rangle \langle Etc\rangle (<X>) <c2>
\]

\[
\langle Measure\rangle \rightarrow \langle Number\rangle \langle Ordinal\rangle \mid \text{percent} \mid \text{times} \mid \text{half} \mid \text{again} \mid \text{twice} \mid \text{again}
\]

\[
\langle Etc\rangle \rightarrow \text{half} \mid \text{third} \mid \text{thirds} \mid \ldots
\]

\[
\langle Comp\rangle \rightarrow \langle NF\rangle \langle Etc\rangle
\]

\[
<c1>/<c2> \rightarrow \text{less/than} \mid \text{less/than} \mid \text{as/as}
\]

where (...) denotes optionality; */ indicates "agreement" between comparative particles; and \langle Etc\rangle accounts for items parallel to those in the matrix clause in which the comparative occurs (e.g. "cars that are longer than the Regal is (wide)"). In addition, a variety of extrapositions (i.e. rightward
and occasional leftward movement) from C< X > may (and sometimes must) occur. For example, both "cars larger than the Century" and "larger cars than the Century" are allowed.

Since we wish to allow C< X > structures to occur wherever < X > could occur, arbitrarily complex interactions with quantifiers (within the complement), ordinals, superlatives, raisings, wh elements, and other constructs must be provided for. In addition to the structures indicated by the BNF above, we allow for some simpler expressions not conventionally classified as comparatives. Some examples are "6 cars" (cf. "as many as 6 cars") and "3 inches long" (cf. "as long as 3 inches"). We also provide for structures involving the nominal counterpart of an adjective, as in "more than 185 inches in length".

To date, we have fully implemented a wide variety of comparatives related to adjectives, quantifiers, and measure nouns (e.g. "cars that cost at least $100 more than the Park Avenue"). Due to the commonality among the comparativized syntactic structures, our grammar for these three types of comparatives is produced by meta-rules suggested by the BNF rules shown above. Although the feature agreement provided by our parser is used to eliminate spurious structures such as "cars more than 3 (inches/*dollars) long", we avoid conflicts between pure numbers and measure phrases that involve a unit (e.g. "companies that make more than 3 (*dollars) cars") by having two (very nearly identical) Quantity routines in the grammar.

1.3 Limitations

In addition to some specific limitations to be stated in the remainder of the paper, there are some general limitations of our work to date, many of which are being rectified by the work mentioned in Section 8.3. (1) By analogy with conjunctions, with which comparatives share a number of properties (cf. Sager 1981, pp. 196ff), our comparative particle pairs (-er/than etc.) provide for co-ordinate comparatives, in contrast to pairs such as so/that, as in "Buick makes so many cars that it's the largest company." (2) Comparative complements are expected in a limited number of places. For example, "Audi makes more large cars than Pontiac in France" is recognized but "Audi makes more large cars in France than Pontiac" is not. This is because we currently propagate the evidence of having found a comparative particle ("more") to the noun phrase headed by "cars", hence the complement ("than ...") can attach there, but not to the higher level verb phrase headed by "makes".

This limitation also prevents our processing "What companies make a larger car than Buick", whose exact meaning(s) the reader is invited to ponder. (3) Since comparative complements are based on noun phrases, neither "Audi makes more large cars in France than in Germany" nor "Audi makes large cars more in France than in Germany" is recognized. (4) We attempt no pragmatic disambiguation of semantically ambiguous comparatives. Thus, when confronted with "more than 3 inches shorter" or "more than 3 fewer cars", we provide the compositional interpretation associated with our left recursive syntax. Even expressions such as "as many" and "as large" are ambiguous between at least and exactly. (5) We attempt no anaphora processing, and so comparatives without a complement, as in "Which cars are larger?", are not processed. (6) We provide general conversion of units of measure (e.g. "2 feet longer" is the same as "24 inches longer") but they are not fully incorporated into the system.

2. An Initial Example

The mechanisms we shall describe apply a conventional series of transformations to sentences containing one or more comparatives, ultimately resulting in an executable expression. As an example of this process, we'll consider the input

"List the cars at least 20 inches more than twice as long as the Century is wide"

which contains a highly comparativized adjective. First, this input is scanned and parsed, yielding the parse tree shown in Figure 1. Note that each COMPAR node has a QUANTITY node and a MODE of its own. Also, the MODE of the top COMPAR (whose value is "equal") is co-indexed (indicated by the subscript i) with the MODE feature associate with the particle ("as") that intervenes between the ADJ and its COMPAR-ARG; this assures that -er/than, less/than, and as/as pairs collocate correctly. Next, we build a "normalized" parse tree by reconstructing elements that were discontinuous in the surface structure and

2. A formal account the associated formalisms, including a BNF syntax and a denotational semantics for our "normalized parse trees" and "algebraic-logical form" language, is given in Ballard and Stumberger (1987).

3. Dashed lines indicate features, as distinct from lexical items, and empty nodes, which result from Whiz-deletion, are denoted by "?".
by performing other simplifications. This yields the following structure, whose 2-place predicate, with P (parameter) and A (argument) as variables, corresponds to "at least 20 inches more than twice as ... as".

Normalized Parse Tree:
(CAR (NOUN CAR)
   (COMPAR (ADJ LONG)
      (λ (P A) (≥ P (* 20 (* 2 A))))
      (CAR (= CENTURY))
      (ADJ WIDE)))

Next, user-defined meanings of words and phrases are looked up and the comparativization operations described in Section 6 are performed, yielding

Algebraic-Logical Form:
(SET (CAR P1)
   (≥ 20 (* 2 (WIDTH-OF-CAR CENTURY)))
)

Finally, this representation is converted into the executable expression indicated by

Final Executable Expression:
(SUBSET (λ (P1)
   (≥ (KSV P1 @S{LENGTH})
      158)
   (KI @F{CAR})))

where KSV and KI are primitive retrieval functions of the Kandor back-end; @I{...}, @F{...} and @S{...} are Lisp objects respectively denoting instances, frames, and slots in Kandor's taxonomic knowledge base; and ≥ is a coercion routine supplied by TELI to accommodate backend retrieval system that produce numbers in disguise (e.g. a Lisp object or a singleton set) on which the standard Lisp functions would choke. However, since compositionally created structures such as the preceding one are often intolerably inefficient, optimizations are carried out while the executable expression is being formed. In the case at hand, the second argument of ≥ is constant, so it is evaluated, producing

Optimized Executable Expression:
(SUBSET (λ (P1)
   (≥ (KSV P1 @S{LENGTH}) 158))
   (KI @F{CAR})))

A second example, which illustrates a comparative quantifier, is given in an appendix where, as a result of optimizations analogous to those which produced the constant 158 above, the comparative "at least 3 more large cars than Buick" is eventually processed exactly as though it had been "at least 6 cars" (since Buick made 3 large cars).

3. Lexical Provisions for Comparatives

Our current repertoire of domain-independent lexical items associated with comparatives includes "many", "few", and "much"; "more", with 3 readings (er, er+many, er+much), following Bresnan (1972) and similar to Robinson (1982, p. 28); "fewer (er+few); "less", with 3 readings (less, er+few, less+much); several formatives and adverbials ("at", "least", "most", "exactly", "precisely", "only", "just", "half", "again", "times", "percent"); and a handful of spelled-out ordinals ("thirds" etc.). Though not stored in the lexicon, both integers and floating-point numbers (cf. "3.45 inches") are also involved in comparativization.

The domain-dependent portion of the lexicon includes members of the open categories of adjectives, measure nouns, and comparative inflections of adjectives. The scanner output for the comparative of the adjective A is er+A (e.g. "larger" becomes er+large).

4. Syntax for Comparatives

The basic syntax for comparatives adheres to the meta-rules given in Section 1.2. As indicated in the parse tree of Figure 1, COMPAR is never a primary tree node but is instead a daughter of the node being comparativized. Furthermore, since our grammar has recently taken on somewhat of an X-bar flavor (cf. Jackendoff, 1977), the complement for a comparativized item is found as either its sister or its parent's sister. Complex comparatives derive from left-recursive structures. Our present grammar for comparatives is set up partly by meta-rules and partly by hand-coded rules relating to such idiosyncrasies as "more than 3 inches in length" (however, cf. "more than 6 in number").

6. To the possible horror of the prescriptive grammarian, this accounts for such atrocities as "less books".

7. Though our parser operates top-down, we've incorporated a general mechanism for left recursion that's also utilized by possessives (e.g. "the newest car's company's largest competitor's smallest car").

8. Meta-rules are also used to produce the grammar for relative clauses, yes-no questions, and a host of other structures (e.g. various slash categories) from a hand-coded grammar for basic declarative sentences.
Letting Node{<X>} denote a node of the normalized parse tree associated with an element of type <X>, comparatives involve the replacement denoted by

\[
\text{Node}[\text{COMPAR Node}{<X>} <\text{Rel}> <\text{Arg}> <\text{Etc}_X>]
\]

where <Arg> corresponds to an optional noun phrase, <Etc>_X captures non-elided material associated with the matrix clause, and the 2-place-relation denoted by <Rel> is the most interesting (and by far the most complex) element produced. The algorithm that produces it converts "more", "less", and "times" respectively into +, -, and *. This process is left recursive; the relational operator is determined from the highest MODE, and by default it is assigned to be =.9 As indicated below, these algebraic and arithmetic symbols will be preserved in the executable expression unless the word being comparativized indicates a downward direction on the scale applicable to it (e.g. "fewer", "shorter"), in which case they will be reversed (e.g. \( \geq \) becomes \( \leq \) and \( + \) becomes \( - \)). Each 2-place-relation is the body of a 2-place lambda whose variables, P and A, are associated with values obtained from a parameter and an argument against which a comparison is being made. Some example 2-place-predicates are

- more than 166 inches long
- more than 15 feet long
- at least 180 inches long
- longer than (\( \geq \) P A)
- at least as long as (\( \geq \) P A)
- 1 inch longer than (\( \geq \) P (+ 1 A))
- exactly twice as long as (\( \geq \) P (+ 3 A))
- 3 times as long as (\( \geq \) P (+ 1.5 A))
- half again as long as (\( \geq \) P (+ (+ / 40 100) 1 A))
- forty percent longer than (\( \geq \) P (+ (\( -\) 0.4 A) A))
- less than one third as long as (\( \leq \) P (+ (\( -\) 0.3 A) A))
- at least 3 inches more than (\( \geq \) P (+ 3 (+ 2 A)))

When the measure noun appearing in an English input differs from that by which the objects being tested are measured, as indicated by the second example above, a scalar conversion is required.

The semantics of comparativization involves converting a one-place predicate into another one-place predicate by performing arbitrarily complex operations on it. For example, if "large car" has been defined as a car whose length exceeds 190 inches, then, letting "A" denote a noun phrase complement, some examples are

\[
\begin{align*}
\text{long} & \quad \text{Length}(x) \geq 190 \\
\text{longer than 180 inches} & \quad \text{Length}(x) > 180 \\
\text{longer than A} & \quad \text{Length}(x) > \text{Length}(A) \\
\text{no longer than A} & \quad \text{Length}(x) \leq \text{Length}(A) \\
\text{twice as long as A is wide} & \quad \text{Length}(x) \geq 2 \cdot \text{Width}(A) \\
\text{3 inches more than twice as long as A} & \quad \text{Length}(x) > 3 + 2 \cdot \text{Length}(A)
\end{align*}
\]

where each of these right-hand-sides is the body of a one-place predicate whose single variable is x.

As a second example, comparative quantifiers such as "more than 6" are handled by an identical process10, as indicated by11

\[
\begin{align*}
\text{x has many y's} & \quad \text{Size} \{y \mid \text{Has}(x,y)\} > \text{Constant} \\
\text{x has more than 6 y's} & \quad \text{Size} \{y \mid \text{Has}(x,y)\} > 6 \\
\text{x has more y's than A} & \quad \text{Size} \{y \mid \text{Has}(x,y)\} > \text{Size} \{y \mid \text{Has}(A,y)\} \\
\text{x has at least 2 more} & \quad \text{Size} \{y \mid \text{Has}(x,y)\} > 2 + \text{Size} \{y \mid \text{Has}(A,y)\}
\end{align*}
\]

where the initial Constant denotes some arbitrary constant.

In general, comparativizing a one-place predicate takes place as follows.

1. Find (a) an appropriate one-place function and (b) an associated relational operator that tells which direction on a linear scale indicates having "more" of the property.

2. Apply the relational operator located above to the modality of the comparison to determine the relational operator that will appear in the IR+. If the relational operator of the definition being comparativized is either \( \geq \) or \( \geq \), use the mode occurring in the IR; otherwise, "reverse" the mode by doing what would be a negation but leaving untouched the = portion of the operator. Thus, the reversal of \( < \) is \( > \), the

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9. This addresses the inherent ambiguity of as/as structures without an adverbial element, such as "exactly" or "at least". Thus, "people with 3 children" is interpreted as people with exactly 3 children.

10. That is, we have no special purpose processing for "more than", "how many" etc.

11. We use "has" in these examples for clarity; naturally, the scope of a comparative quantifier may contain an arbitrarily complex predicate.
reversal of $\leq$ is $\geq$, and so forth. Similarly, $+$ and $-$ are switched.

3. Determine the argument being compared against (possibly a constant).

4. Link these pieces together. If the argument was not constant (e.g. "... longer than at least 3 foreign cars"), wrap its scope around the resulting expression.

For example, if "short car" has been defined as

*x is short*: \(\text{Length}(x) \leq 160\)

then the 1-place function and relational operator are determined in step 1 to be \(\text{Length}\) and \(\leq\), and thus we have

"shorter than A" \(\rightarrow\) \(\text{Length}(x) < \text{Length}(A)\)

"exactly 3 inches shorter than A" \(\rightarrow\) \(\text{Length}(x) = \text{Length}(A) - 3\)

7. Comparatives Containing a Wh Element

In addition to recognizing wh elements associated with a relative or interrogative clause,\(^{12}\) TELI recognizes the word how when it appears in place of a quantity, e.g. "how long" (cf. "6 inches long") and "how many more" (cf. "6 more"\(^{13}\)). Wherever how appears, however, we treat its semantics as roughly "solve for how such that". In the case of interrogative pronouns (e.g. "what"), this leads rather obviously to an internal representation asking for a SET. In the case of how, this treatment is also in order since it represents a (quantity) NP. For simplicity, we produce an expression containing an unbound wh and later give it wide scope.\(^{14}\) In particular, subsequent processing involves moving the wh element upward in the logical form tree\(^{15}\) by performing appropriate transformations.

For illustration, consider the absurdly complicated example

"Buick makes \(3\) more than how many percent more cars than Audi?"

the comparative portion of whose internal representation\(^{16}\) is

\[
\lambda (P \; A) \; ([= \; P \; (\times \; (\times \; A \; (+ \; 1 \; (/ \; \text{WH} \; 100)) \; 3)]
\]

At this point, we proceed with semantic processing, ignoring for the moment the presence of the unbound WH element. In the case at hand, this leads to

\[
\begin{align*}
&= \; \text{COUNT} \; (\text{SET} \; (\text{CAR} \; \text{P1}) \; (\text{Make} \; \text{BUICK} \; \text{P1})) \\
&\times \; (\text{COUNT} \; (\text{SET} \; (\text{CAR} \; \text{P1}) \; (\text{Make} \; \text{AUDI} \; \text{P1}))) \\
&\times \; (1 \; (/ \; \text{WH} \; 100))) \\
&3)
\end{align*}
\]

after which we "solve for" WH to yield

\[
\begin{align*}
&\times \; (- \; (/ \; (- \; \text{COUNT} \; (\text{SET} \; (\text{CAR} \; \text{P1}) \; (\text{Make} \; \text{BUICK} \; \text{P1}))) \\
&\times \; (\text{COUNT} \; (\text{SET} \; (\text{CAR} \; \text{P1}) \; (\text{Make} \; \text{AUDI} \; \text{P1}))) \\
&3)) \; 100)
\end{align*}
\]

This process is not dependent on the position in which the wh occurred, and thus takes the place of special-purposes interpretation routines for "how many", "How <Adjective>", and so forth.\(^{17}\)

8. Discussion

Thus far, we have presented an overview of our treatment of comparatives, with as much detail as we're able to supply in a conference-length paper. Although we can offer no substantive empirical evidence with TELI (e.g. results of use by non-authors), we believe some of the techniques we've presented can be put to use by the reader. Further information, especially with regard to the interaction of comparatives with a variety of other types of constructs, can be found in Ballard and Stumberger (1987).

\[^{12}\] To see that wh is less than a "word", consider pairs such as what/that, where/there and when/then. The advantage of recognizing sub-word units as the primitives on which syntax and/or semantic analysis is based should come as no surprise to anyone acquainted with the structure of languages other than English, which is unusual in coming so close to being treatable solely at the word level.

\[^{13}\] As stated earlier, we have adopted derivations suggested by Brennan (1973) such as -er+many---qore. In the case at hand, we must assume something like Q+many---Q, where Q denotes a quantity.

\[^{14}\] The scope is wide but not global because of inputs such as "How many cars does each US company make?"

\[^{15}\] Of course, our algebraic-logical forms, based on operators and their associated arguments, amount to being trees.

\[^{16}\] The sentence is ambiguous, with readings indicated by "3 more than [how many percent]" and "[3 more than how many] percent". As indicated earlier, we presently take the reading that favors the use of left recursion.

\[^{17}\] Problematic situations can arise in which simple algebraic operations aren't sufficient. For example, in examples such as "Cars were sold to people with how many children?", we must move wh past a logical quantifier, rather than the arithmetic operators as shown above.
8.1 Related Work

Although the literature describing implemented NL processors contains many examples of comparative constructions (cf. Kirsch (1964) for a wealth of early examples), at least two qualifications may be given concerning the current "state of the art" of comparative treatment. First, the majority of the examples appearing in the literature are quite simple 18 (e.g. "more than $250") and can be prepared for by specifying a 2-place predicate in advance that's effectively equivalent to the 2-place predicate we construct from an underlying 1-place predicate by way of coercion into a 1-place function. This allows one to avoid some slippery problems of movement (which we have addressed but have certainly not disposed of), to ignore morphological subtleties (e.g. recognizing the "er" of "larger" or "more" as -er, a "word" to be input to the parser), and to take other shortcuts. 19 Second, although examples of various types of comparatives are not hard to come by, accounts of the actual mechanisms that treat comparatives are harder to find, as are specific statements of the generality which authors believe themselves to have provided for.

8.2 Levels of Representation

The architecture of TELI resembles that of similarly motivated question answering systems (cf. Grosz et al, 1987; Hafner and Godden, 1985; Bates and Bobrow, 1983 and Bates et al 1985) by comprising a linear sequence of processing stages which produce successively "lower" level representations of the input. 20 Although our parse tree format is rather conventional, 21 what we have called "normalized parse tree" and "algebraic-logical form" correspond rather loosely to what in the literature are often called "logical form" and "meaning representation", respectively. Furthermore, in the most recent work with TELI, meaningful distinctions between modules have become blurred, although the relative order in which operations are carried out is largely the same.

In seeking to compare our formalisms and processing strategies with others that have been proposed, we have found terms such as "logical form" being used in the literature in quite vague and often incompatible ways. Furthermore, we know of no compelling arguments that suggest that a psychologically plausible model of human information processing will require intermediate levels such as parse trees, logical forms, and the like. Is it even clear that there ought be be a finite number of successive "levels", whatever they might be? We are increasingly doubtful that the trappings spawned by linguists and philosophers can be put in a bag, sprinkled with Common Lisp, shaken, and expected to yield robust natural language processors. More of an interdisciplinary effort may be required than has yet been seen.

8.3 Current Work

The representation given in Section 5 fundamentally restricts us from handling comparatives whose complement is more than one level above the word being comparativized (e.g. "John persuaded his students to contribute to more museums than Bill did"). Our current work involves producing normalized parse tree structures of roughly the form

\[(\text{COMPAR-2} \ C_i <\text{Comp}>\]

\[\ldots (\text{COMPAR-1} \ C_i \ldots) \ldots \]

where the COMPAR-1 and \(<\text{Comp}>\) structures correspond to the COMPAR structure given in Section 5; \(C_i\) provides for co-indexing when multiple comparativizations are present; and the first "\ldots" allows for arbitrarily many levels. This calls upon us to modify the semantic processing presented in Section 6, making it resemble the treatment given to wh elements as described in Section 7.

9. Conclusions

We have presented algorithms aimed at the morphological, syntactic, and semantic problems associated with a large variety of comparative structures that arise in the context of question answering. We believe the extent of our coverage equals in several ways and exceeds in some ways the capabilities known to us via the literature. However,
comparatives operate as a "meta" phenomenon and thus cut across many issues; we have ignored certain problems and knowingly treated others inadequately. Further work is certainly required, and we hope to have presented a framework in which (1) some interesting and important capabilities can be provided for now and (2) further computational studies can be carried out.

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Appendix: Processing a Comparative Quantifier

English Input:
"Have any US companies made at least 3 more large cars than Buick?"

Normalized Parse Tree:

```
| vP | np (company make car nil nil nil) |
| subj | (company (adj us)) |
| obj | (obj (car (compar (quant more) (more 2))|
| (company (= buick))) |
| (car (adj large)) |
| (noun car))))
```

Algebraic-Logical Form:
```
(quant (company p1) (more 2))
```
```
1. (and (ki (pi atm)) (and (ki (pi atm)) (ki (pi atm))))
2. (gpc-count (subset (a) (p2)) (and (ki (pi atm)) (ki (pi atm))))
3. (gpc-count (subset (a) (p2)) (and (ki (pi atm)) (ki (pi atm))))
```

Final Executable Expression:
```
(gpc-some '(1 c4))
```
```
(lambda (p1)
  (and (ki p1 (gpc (= us company))))
  (gpc-count (subset (a) (p2)) (and (ki (pi atm)) (ki (pi atm))))
  (gpc-count (subset (a) (p2)) (and (ki (pi atm)) (ki (pi atm))))
)
```

Optimized Executable Expression:
```
(gpc-some '(1 c4))
```
```
(lambda (p1)
  (gpc-some '(6 c4))
  (and (ki p1 (gpc (= us company))))
  (and (ki p1 (gpc (= us company))))
)
```
```
48