Understanding Polarized Dust Emission from $\rho$ Ophiuchi A in Light of Grain Alignment and Disruption by Radiative Torques

Le Ngoc Tram$^{1,2}$, Thiem Hoang$^{3,4}$, Hyeseung Lee$^3$, Fabio P. Santos$^5$, Archana Soam$^1$, Pierre Lesaffre$^6,7$, Antoine Gusdorf$^6,7$, and William T. Reach$^1$

1 Stratospheric Observatory for Infrared Astronomy, Universities Space Research Association, NASA Ames Research Center, MS 232-11, Moffett Field, 94035 CA, USA; ngoctram.le@nasa.gov
2 University of Science and Technology of Hanoi, VAST, 18 Hoang Quoc Viet, Vietnam
3 Korea Astronomy and Space Science Institute, Daejeon 34055, Republic of Korea
4 Korea University of Science and Technology, 217 Gajeong-ro, Yuseong-gu, Daejeon, 34113, Republic of Korea
5 Max-Planck-Institute for Astronomy, Königstuhl 17, D-69117 Heidelberg, Germany
6 Laboratoire de Physique de l’École normal supérieur, ENS, Université PSL, CNRS, Sorbonne Université, Université de Paris, France
7 Observatoire de Paris, PSL University, Sorbonne Université, LERMA, F-75014, Paris, France

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Abstract

The alignment of dust grains with the ambient magnetic field produces polarization of starlight as well as thermal dust emission. Using the archival SOFIA/HAWC+ polarimetric data observed toward the $\rho$ Ophiuchus (Oph) A cloud hosted by a B star at 89 and 154 $\mu$m, we find that the fractional polarization of thermal dust emission first increases with the grain temperature and then decreases once the grain temperature exceeds $\approx$25--32 K. The latter trend differs from the prediction of the popular RAdiative Torques (RATs) alignment theory, which implies a monotonic increase of the polarization fraction with the grain temperature. We perform numerical modeling of polarized dust emission for the $\rho$ Oph-A cloud and calculate the degree of dust polarization by simultaneously considering the dust grain alignment and rotational disruption by RATs. Our modeling results could successfully reproduce both the rising and declining trends of the observational data. Moreover, we show that the alignment of only silicate grains or a mixture of silicate–carbon grains within a composite structure can reproduce the observational trends, assuming that all dust grains follow a power-law size distribution. Although there are a number of simplifications and limitations to our modeling, our results suggest grains in the $\rho$ Oph-A cloud have a composite structure, and the grain size distribution has a steeper slope than the standard size distribution for the interstellar medium. Combination of SOFIA/HAWC+ data with JCMT observations 450 and 850 $\mu$m would be useful to test the proposed scenario based on grain alignment and disruption by RATs.

Unified Astronomy Thesaurus concepts: Interstellar radiation field (852); Interstellar dust (836); Interstellar medium (847); Interstellar dust extinction (837); Polarimetry (1278)

1. Introduction

The magnetic field is believed to play an essential role in various astrophysical phenomena, including the formation of stars and planets (Crutcher 2012). The alignment of dust grains with the magnetic field induces polarization of starlight and of thermal dust emission. The polarization vectors of starlight are parallel to the magnetic field, while those of thermal dust are perpendicular to the magnetic field. Thus, dust polarization has become a popular technique to constrain the magnetic field direction and strength (Lazarian 2007; Andersson et al. 2015).

Observations have reported an anticorrelation trend of the fractional polarization of thermal dust emission with the column density of the gas in molecular clouds (e.g., Arce et al. 1998; Whittet et al. 2008; Planck Collaboration et al. 2015, 2020; Fissel et al. 2016; Santos et al. 2017, 2019; Chuss et al. 2019). This trend is explained by the loss of grain alignment toward dense cores (Whittet et al. 2008; Hoang et al. 2020) or by the turbulent structure of magnetic field within the scale of the beam size (see Jones & Whittet 2015; Planck Collaboration et al. 2015).

A popular theory describing grain alignment is RAdiative Torques (hereafter referred to as RATs; Lazarian & Hoang 2007; see Lazarian 2007; Andersson et al. 2015 for reviews). One of the key predictions of the RAT theory is that the polarization degree correlates with the intensity of the radiation field (or equivalently dust temperature $T_d$). This prediction was numerically demonstrated by Lee et al. (2020). However, observations revealed that the dust polarization degree does not always increase with $T_d$. For example, Planck Collaboration et al. (2020) showed that the 40' spatial resolution polarization degree at 850 $\mu$m, measured by the Planck satellite toward five molecular regions, including Aquila Rift, Cham-Musca, Orion, and Ophiuchus in the Gould belt cloud, decreases for $T_d > 19$ K (see their Figure 18). Additionally, far-infrared polarimetric data observed by the High-resolution Airborne Wide band Camera Plus (HAWC+) instrument (Harper et al. 2018) on board the Stratosphere Observatory for Infrared Astronomy (SOFIA) toward the molecular cloud Ophiuchus A (Santos et al. 2019) at 89 $\mu$m ($7^{'}8$ spatial resolution) and 154 $\mu$m (13''6 spatial resolution) also reported the decrease of the polarization degree for $T_d > 25$--32 K (see Section 2 below). These observational features are challenging the popular RAT alignment theory.

Dust grain size distribution is an important parameter when it comes to interpreting the polarization of dust. The grain size distribution is expected to evolve from the diffuse interstellar
medium (ISM) to dense molecular clouds (MCs) due to grain accretion of gas species and grain–grain collisions (Hirashita & Li 2013). Recently, Hoang et al. (2019) discovered that a large grain exposed to a strong radiation field could be disrupted into small fragments due to centrifugal stress induced by suprathermal rotation by RATs. This effect is termed Radiative Torques Disruption (RATD; see Hoang 2020 for a review). Since RATs are stronger for larger grains (Lazarian & Hoang 2007; Hoang & Lazarian 2008), RATD is more efficient for large grains than smaller ones. As shown in Hoang (2019), the RATD mechanism is much faster than grain shattering and thus determines the upper cutoff of the grain size distribution in the ISM.

Lee et al. (2020) carried out numerical modeling of multiwavelength polarization of thermal dust emission from aligned grains by RATs. They show that the polarization degree at 850 μm first increases with increasing dust temperature. However, when RATD is accounted for, they find that the polarization degree decreases for higher dust temperature, which is different from the RATs prediction. The level of the decline is found to depend on the tensile strength, which is determined by the internal structure of dust grains (Hoang 2019). Interestingly, accounting for RATD, the model predicts the same $P_d(%) - T_d$ trend as reported by Planck data (Planck Collaboration et al. 2020) at the same wavelength as mentioned above. The success of the joint effect of RAT alignment and RATD in explaining Planck data motivates us to use this approach to better interpret the SOFIA/HAWC+ data.

Coming back to the SOFIA/HAWC+ observation toward ρ Oph-A at bands C (89 μm) and D (154 μm) as mentioned above, Santos et al. (2019) mainly studied the variation of the ratio of the polarization degree ($P_d(%) / P_c(%)$) with respect to the dust temperature, which is opposed to the polarization degree studies. Furthermore, the authors showed that the RATs mechanism was able to explain the increasing (e.g., positive) part of the ratio curve and discarded the decreasing (negative) part (see their Figure 6(d)). In this study, we will (1) use this data set to show the correlation to the polarization degree itself to dust temperature and (2) extend the improved polarized thermal dust model introduced by Lee et al. (2020) to interpret these SOFIA/HAWC+ observational trends.

This paper is structured as follows. We present the archival SOFIA/HAWC+ data from ρ Oph-A at 89 μm and 154 μm observed by SOFIA/HAWC+ in Section 2. We describe our modeling method of polarized thermal dust emission by aligned grains in Section 3. In Section 4, we compare our numerical results obtained for ρ Oph-A cloud with observational data. A summary of our findings and conclusions are presented in Section 5.

2. Observations toward ρ Oph-A

ρ Oph-A is a molecular cloud in one of the closest dark cloud complexes and star-forming regions, ρ Ophiuchi. The distance to this complex is reported to be ~120–160 pc (Chini 1981; de Geus et al. 1989; Knude & Hog 1998; Rebull et al. 2004; Loinard et al. 2008; Lombardi et al. 2008; Mamajek 2008; Snow et al. 2008; Ortiz-León et al. 2017). This region is significantly influenced by high-energy radiation from a high-mass Oph-S1 star, which is a B association star (Vrba 1977; Andre et al. 1988; Loren 1989a, 1989b; Hamaguchi et al. 2003). Among several dark cloud cores in ρ Ophiuchi, Oph-A is identified as one of the warmest cores compared to Oph-B and -C regions. Several studies, i.e., Herschel, Spitzer, and James Clarke Maxwell Telescope (JCMT) Gould belt surveys (Ward-Thompson et al. 2007; Evans et al. 2009; André et al. 2010), include this region for various investigations on dust and gas properties. This cloud complex is also widely studied in multiwavelength imaging and polarimetry. Recent attempts were made to map magnetic fields in the Oph-A region using near-IR and submillimeter polarization measurements by Kwon et al. (2015, 2018) and far-IR by Santos et al. (2019), respectively. Oph-A is one of the best laboratories to understand the multiband dust polarization in the context of high-energy radiation giving us an opportunity to investigate RAT in detail.

2.1. Polarization Maps

In this work, we use the archival FIR polarimetric data observed by SOFIA/HAWC+. These data sets are introduced in Santos et al. (2019). The observations were made in 2017 using two bands of HAWC+ instrument, namely C (89 μm) and D (154 μm). The angular resolutions are 7′′8 and 13′′6, respectively. The polarization degree maps in these bands are shown in Figures 1(a) and (b). 8 We select the common sky positions in which data is detected in both bands. The local polarization degree varies significantly across the ρ Oph-A cloud, in which the median value is 7.5% in band C and 5.0% in band D as discussed in Santos et al. (2019). Figures 1(a) and (b) show a “tight” spatial correlation in polarization degree in two bands except at the southernmost area ($T_d \approx 25$ K), where the data at 89 μm is more polarized than at 154 μm. The reason for this difference is beyond this work’s scope because we do not have enough information to investigate it quantitatively. However, a possible explanation could be that there is a warmer outer component (with a local temperature larger than 25 K) and a colder inner component (with a local temperature smaller than 25 K) along the line of sight (LOS) as proposed in Santos et al. (2019). In the warmer component, which favors enhancing the shorter wavelength polarization (band C), grains are well exposed to radiation. Therefore the alignment is efficient, causing a larger value of $P_c(%)$. On the contrary, the colder component along the LOS favors emission at longer wavelengths (band D); however, the grain alignment is less effective due to the shielding. Therefore, the value of $P_d(%)$ becomes smaller. A star symbol indicates the high-mass star Oph S1.

2.2. Map of Dust Temperature and Gas Density

We adopt the dust temperature ($T_d$) and the gas column density ($N$) maps of Santos et al. (2019). These maps were generated by a fit of the modified thermal spectral energy distribution (SED) to each pixel using 70, 100, and 160 μm from Herschel/PACS data (Poglitsch et al. 2010) with the fixed exponential index of the dust opacity 1.6. Figures 1(c) and (d) show the gas density and dust temperature maps in the same regions that HAWC+ detected data. The high-mass star Oph S1 warms up the surrounding environment, causing a large temperature gradient, i.e., from $\sim$45 K near Oph S1 down to $\sim$20 K at the edge of the cloud. On the contrary, the gas is densest at the edge of the map and radially diffuses backward to Oph S1.

8 We smoothed the 7′′8 band C and the 11′′4 dust temperature maps to 13′′6 band D resolution using the python-package GAUSSIAN2DKERNEL.
2.3. Dust Polarization and Temperature

Figure 2 shows the 2D-histogram dust polarization degree in bands C (left panel) and D (right panel) to dust temperature made of 52 bins. They share the same feature (1) the polarization degree increases as the dust temperature increases up to \( T_d \approx T_{\text{crit}} \) (i.e., positive slope region) and (2) the polarization degree decreases for higher dust temperature (i.e., negative slope region). In the positive slope, the polarization degree in band C is higher than that in band D, while it is lower in the negative slope, which was also shown by the fractional polarization ratio of Figure 6(d) in Santos et al. (2019). In other words, the polarization degree at a shorter wavelength (89 \( \mu \text{m} \)) is higher than at the longer wavelength (154 \( \mu \text{m} \)) in the denser region (i.e., at the edge of the polarimetric map) while it is the opposite in the less dense region (close central star) in \( \rho \text{ Oph-A} \). Using the RATs theory, the spherical model of Santos et al. (2019) could explain the increase (decrease) of the \( P_D/P_C \) ratio with respect to dust temperature (gas column density) in the dense (\( N > 10^{21.75} \text{ cm}^{-2} \)) and cold region (\( T_d \leq 32-34 \text{ K} \)) (see their Figure 6). However, this model could not explain the observational trend in the more diffuse and hotter region. We fitted the data with a piecewise linear function. The best fits (i.e., black dashed lines) show that the transition takes place at \( T_{\text{crit}} \approx 25 \text{ K} \) for band C, and \( \approx 32 \text{ K} \) for band D. In the statistical point of view, the reason for low \( T_{\text{crit}} \) in band C is that there is an excess of the polarization degree at \( T_d \approx 25 \text{ K} \) as mentioned in Section 2.1, which makes the piecewise linear fit peak toward this value of \( T_d \). In the framework of our theoretical point of view, however, the transition from positive to negative slope at \( \approx 32-34 \text{ K} \) is unlikely physical because the tensile strength of grains must be extremely small (see Section 4). In addition, the polarization ratio \( P_D/P_C \) changes its slope at \( T_d \approx 32-34 \text{ K} \) as shown in Santos et al. (2019).

3. Modeling Thermal Dust Polarization

The multiwavelength polarization model of the thermal dust emission is described in detail in Lee et al. (2020). The schematic of the model is illustrated in Figure 3. The radiative

\( \text{Figure 1. Maps of polarization degree and dust temperature of } \rho \text{ Oph-A. Panels (a) and (b): the polarization degrees measured by bands C and D of HAWC+/SOFIA in the actual resolutions. Panels (c) and (d): the maps of the H}_2 \text{ column density (}N\text{) and the dust temperature (}T_d\text{) derived from 70, 100, and 160 } \mu \text{m Herschel/PACS data. The star symbol locates the position of Oph S1. The black filled circles show the beam size. The physical scale is derived from 140 pc of distance.} \)}
source (e.g., a O/B star) is denoted by a star symbol surrounded by a cloud. The radiative strength ($U$) gets smaller further in the cloud. As follows, we describe the model to calculate the polarization of thermal dust emission from this cloud.

### 3.1. Fractional Polarization of Thermal Emission

Dust grains are heated by the radiation and re-emit in the thermal range. The fractional polarization of the thermal dust emission is the ratio of the polarized intensity ($I_{\text{pol}}$) to the total emission intensity ($I_{\text{em}}$), which yields

$$P(\%) = 100 \times \frac{I_{\text{pol}}}{I_{\text{em}}}. \quad (1)$$

Assuming a dust environment containing carbonaceous and silicate grains, the total emission intensity is given by

$$\frac{I_{\text{em}}(\lambda)}{N_H} = \sum_{j=\text{sil,car}} \int_{a_{\text{min}}}^{a_{\text{max}}} Q_{\text{ext}} \pi a^2 \times \int dT_B(T_d) \frac{dP}{dT} \frac{1}{n_H} \frac{dn_{a\ell}}{da}. \quad (2)$$

If silicate and carbon are separated populations, then as paramagnetic grains, silicates can align with the ambient magnetic field, while carbon grains cannot (Hoang & Lazarian 2016). Thus, the polarized intensity resulting from its alignment is given by

$$\frac{I_{\text{pol}}(\lambda)}{N_H} = \int_{a_{\text{min}}}^{a_{\text{max}}} f(a) Q_{\text{pol}} \pi a^2 \times \int dT_B(T_d) \frac{dP}{dT} \frac{1}{n_H} \frac{dn_{a\ell}}{da}. \quad (3)$$

where $B_S(T_d)$ is the blackbody radiation at dust temperature $T_d$, $dP/dT$ is the distribution of dust temperature, $f(a)$ is the alignment function, $Q_{\text{ext}}$ is the extinction coefficient, $Q_{\text{pol}}$ is the polarization coefficient, and $dn_{a\ell}/da$ is the grain size distribution. The dust temperature distribution depends on the grain size and radiation strength, which is computed by the DustEM code (Compiègne et al. 2011, see, e.g., Figure 8 in Lee et al. 2020). The extinction and polarization coefficients are computed by the DDSCAT model (Draine & Flatau 1994, 2008; Flatau & Draine 2012) for a prolate spheroidal grain shape with an axial ratio of one-third.
If silicate and carbon grains are mixed together (e.g., Jones et al. 2013), which may exist in dense clouds due to many cycles of photoprocessing, coagulation, shattering, accretion, and erosion, carbon grains could be aligned with the ambient magnetic field and its thermal emission could be polarized. For a simplest case, assuming these grain populations have the same alignment parameters (i.e., $a_{\text{align}}, f(a)$), the total polarized intensity is

$$I_{\text{pol}}(\lambda) = \sum_{j=\text{sil,car}} \int_{a_{\text{min}}}^{a_{\text{max}}} f(a) Q_{\text{pol}}(a) d^2 a \times \int dT_B(T_2) \frac{dP}{dT} \frac{1}{n_H} da.$$ (4)

### 3.2. RATD and Grain Size Distribution

Let us consider a radiation field with the energy density of $u_{\text{rad}}$ (erg cm$^{-3}$), the mean wavelength of $\bar{\lambda}$ and an anisotropy degree of $\gamma$. Its strength is defined by a dimensionless $U = u_{\text{rad}}/u_{\text{ISRF}}$, where $u_{\text{ISRF}} = 8.64 \times 10^{-13}$ erg cm$^{-3}$ is the radiation energy density of the interstellar radiation field (ISRF) in the solar neighborhood (Mathis et al. 1983). This radiation field can spin $\alpha$ dust grain of size $a$ and density $\rho$ up to the rotational rate

$$\omega_{\text{RAT}} = 2.9 \times 10^{0.5 \alpha \gamma a^{-3}} U \left( \frac{10^3 \text{cm}^3}{n_H} \right) \frac{\bar{\lambda}}{0.5 \mu\text{m}}^{-1.7} \times \left( \frac{20 \text{K}}{T_{\text{gas}}} \right) \left( \frac{1}{1 + F_{\text{IR}}} \right).$$ (5)

where $a_{\text{min}} = a/(10^{-5} \text{cm})$, $\bar{\rho} = T_{\text{gas}}/(3 \text{gcm}^{-3})$, and $n_H$ and $T_{\text{gas}}$ are the gas density and temperature, $\omega_{\text{RAT}} = (k_B T_{\text{gas}}/I)^{1/5}$ is the thermal angular velocity with $I = 8 \pi r^2 \rho T_{\text{gas}}^4$ is the inertia of the grain. A rotating grain is damped by gas collisions and IR emission (see Hoang 2019). The dimensionless parameter ($F_{\text{IR}}$) that describes the ratio of the IR damping to collisional damping is defined as

$$F_{\text{IR}} \approx 0.4 \left( \frac{U^{2/3}}{a_{\text{min}}} \right) \left( \frac{30 \text{cm}^{-3}}{n_H} \right) \left( \frac{100 \text{K}}{T_{\text{gas}}} \right)^{1/2}.$$ (6)

A grain rotating at rotational velocity $\omega$ results in a tensile stress $S = \rho a^2 \omega^2/4$ on the materials making up the grain. Thus, the maximum rotational velocity that a grain can withstand is:

$$\omega_{\text{crit}} = \frac{2}{a} \left( \frac{S_{\text{max}}}{\rho} \right)^{1/2} \approx 3.6 \times 10^8 \frac{S_{\text{max},7}}{a_{\text{min},7}} \bar{\rho}^{-1/2},$$ (7)

where $S_{\text{max},7} = S_{\text{max}}/(10^7 \text{erg cm}^{-3})$.

One can see from Equation (5) that the stronger the radiation field and the larger the grain size, the faster the rotation of the grain. A strong radiation field can thus generate such a fast rotation that the induced stress on large grains can result in a spontaneous disruption. This disruption mechanism is named as RATD and discovered by Hoang et al. (2019). From Equations (5) and (7), we can derive the critical size above

10 Note that $\omega_{\text{RAT}}/\omega_{\text{crit}} \approx 1/(1 + F_{\text{IR}})$, not $(1 + F_{\text{IR}})$ as the typo in Lee et al. (2020), Equation (3).

11 The factor is corrected to be 0.4 from Equation (4) in Lee et al. (2020).

which grains are disrupted:

$$(a_{\text{disr}}(0.1 \mu\text{m}))^{2.7} \approx 5.1 \gamma_{0.5}^{−1} U^{−1/3} \bar{\lambda}_{0.5}^{1.7} \epsilon^{1/2} \gamma, \label{eq:8}$$ (8)

where $\bar{\lambda}_{0.5} = \bar{\lambda}/(0.5 \mu\text{m})$.

Dust grains are disrupted efficiently (for $a$ greater than $a_{\text{disr}}$) in stronger radiation fields. The disruption of dust grains by RATD can modify the grain size distribution. Since only the largest grains are affected by the RATD mechanism, RATD determines the upper limit of the size distribution. The disruption is thus expected to enhance more smaller grains, resulting in a steeper grain size distribution than in the standard ISM. In the particular case of $\rho$ Oph-A cloud, Liseau et al. (2015) furthermore showed that the grain size distribution experiences a varying power index across the cloud. In this work, we adopt a power-law grain size distribution assumption for both the original large grains and the smaller grains produced by disruption, with a power-law index $\beta$:

$$\frac{1}{n_H} \frac{dn_{\text{sil,car}}}{da} = C_{\text{sil,car}} a^{-\beta} (a_{\text{min}} \leq a \leq a_{\text{max}}).$$ (9)

where $C_{\text{sil}}$ and $C_{\text{car}}$ are the normalization constants for silicate and carbonaceous grains, respectively. The smallest grain size is chosen as $a_{\text{min}} = 10 \AA$, while the maximum size is constrained by the RATD mechanism (i.e., $a_{\text{max}} = a_{\text{disr}}$). The normalization constants are determined through the dust-to-gas mass ratio $M_{\text{d/g}}$ (see Chau Giang & Hoang 2020; Tram et al. 2020) as

$$\sum_{j=\text{sil,car}} C_j \rho_j = \frac{(4 + \beta) M_{d/g} m_{\text{gas}}}{4 \pi (a_{\text{max}}^{4+\beta} - a_{\text{min}}^{4+\beta})} \quad \text{for } \beta \neq -4,$$

$$\sum_{j=\text{sil,car}} C_j \rho_j = \frac{M_{d/g} m_{\text{gas}}}{4 \pi (\ln a_{\text{max}} - \ln a_{\text{min}})} \quad \text{for } \beta = -4,\label{eq:10}$$ (10)

where $C_{\text{sil}}/C_{\text{car}}$ is adopted as 1.12 (Draine & Lee 1984), and the dust-to-mass ratio $M_{d/g}$ is fixed as 0.01 throughout this work. The latter assumption is close to what is derived from X-ray observations $\approx 0.011 – 0.0125$ (Vuong et al. 2003) or gas tracers $\approx 0.0114$ (Liseau et al. 2015).

### 3.3. Grain Alignment by RATs

An anisotropic radiation field can align dust grains via the RATs mechanism (see Lazarian 2007; Andersson et al. 2015 for reviews). In the unified theory of RATs alignment, grains are first spun-up to suprathermal rotation and then driven to be aligned with the ambient magnetic fields by superparamagnetic relaxation within grains having iron inclusions (Hoang & Lazarian 2016). Therefore, grains are only efficiently aligned when they can rotate suprathermally. This aligned grain size ($a_{\text{align}}$) is determined by the following condition $\omega_{\text{RAT}}(a_{\text{align}}) = 3\omega_T$ as in Hoang & Lazarian (2008). From Equation (5), we have:

$$(a_{\text{align}} \approx 0.024 \bar{\rho}^{−5/32} \bar{\lambda}^{−5/16} U^{−5/16} \left( \frac{10^3 \text{cm}^3}{n_H} \right)^{−5/16} \left( \frac{20 \text{K}}{T_{\text{gas}}} \right)^{−5/16} \left( \frac{1}{1 + F_{\text{IR}}} \right)^{−5/16} \mu\text{m}),$$ (11)
which implies $a_{\text{align}} \sim 0.02 \mu m$ for a dense ISM with $\gamma = 1.0$, $U = 1$, and $\lambda = 0.3 \mu m$. In this work, we adopt the alignment function as in Lee et al. (2020):

$$f(a) = \frac{f_{\text{max}}}{1 + (f_{\text{max}} - f_{\text{min}}) \left( 1 - \exp \left( -\frac{0.5a}{a_{\text{align}}} \right)^3 \right)}.$$  

For those grains with $a \ll a_{\text{align}}$, the alignment is minimum as $f_{\text{min}} = 10^{-3}$, while the alignment degree gets maximum $f_{\text{max}}$ for $a \gg a_{\text{align}}$. This parametric function agrees with the results obtained from inverse modeling to interstellar polarization data (Draine & Fraisse 2009; Hoang et al. 2014). For the model with only silicate grains aligned, modeling requires $f_{\text{max}} = 1$, and a mixture model with both carbon and silicate grains aligned requires $f_{\text{max}} < 1$ (Draine & Fraisse 2009; Guillet et al. 2018).

4. Application to $\rho$ Oph-A

4.1. Numerical Setup

As discussed in Section 3, the parameters of the model include the gas properties of gas number density ($n_{\text{H}}$) and gas temperature ($T_{\text{gas}}$); the dust properties of size ($a$), shape, internal structure (i.e., tensile strength $S_{\text{max}}$), and size distribution power index ($\beta$); and the ambient properties of radiation field strength $U$ (which is in fact equivalent to the dust temperature $T_{\text{d}}$), mean wavelength ($\lambda$), and an anisotropy degree ($\gamma$) of the radiation field. Figure 1(c) shows that the gas is denser at the edge of the polarimetric map area and more diffuse close to the Oph S1 star. We derive the relation between the gas number density and the dust temperature by assuming that the dust temperature linearly decreases from 45 K down to 20 K at the edge of the polarimetric map area, and the gas number density is calculated from a spherical model as in Section 3.5 of Santos et al. (2019). This relation is shown in Figure 4. Throughout this work, we fix the value of the gas temperature as $T_{\text{gas}} = 20$ K, which is fairly common for dense molecular clouds.

In a dense molecular cloud, large grains are expected to be present thanks to the coagulation process. We set the initial maximum value of grain size as $1 \mu m$, then the RATD mechanism constrains the actual maximum value. The smallest value for the grain sizes is kept fixed at $10 \AA$. The internal structure of grains is determined via their tensile strength (e.g., large composite grains have $S_{\text{max}} \approx 10^7$ erg cm$^{-3}$, stronger grains have a higher value of $S_{\text{max}}$), which is a free parameter. The grain size distribution could change across the $\rho$ Oph-A cloud (Liseau et al. 2015), thus we vary the power index $\beta$ as another free parameter. In our model, the local value of the radiation strength is determined by the dust temperature as shown in Figure 1(d) via the relation $T_d = 16.4a_1^{-\frac{1}{4}}U_1^{1/6}$K (Draine 2011). The mean wavelength is $\lambda \approx 0.3 \mu m$ corresponding to a B-like star with $T_d \approx 1.5 \times 10^4$ K. The anisotropy degree is $\gamma = 1$ for the unidirectional radiation field from a nearby star.

4.2. Numerical Results

Here, we show the numerical results of the multiwavelength polarization degree of thermal dust emission using RATs theory in two cases: without disruption (namely classical RATs) and with disruption for comparison.

Figure 5 shows the polarization spectra obtained with grain alignment by RATs only (without RATD), computed for several values of the dust temperature with different grain size distributions, i.e., $\beta = -3.5$ (left panel) and $\beta = -4.0$ (right panel). One can see that (1) the polarization degree proportionally increases as the dust temperature increases, and (2) the polarization degree is lower for lower values of $\beta$ for the same $T_d$. The first effect is due to the fact that a higher dust temperature (equivalent to higher radiation strength) causes larger torques acting on dust grains, which decreases the alignment size $a_{\text{align}}$ and then increases the polarization degree of dust emission. Moreover, for a lower $\beta$, the dust mass contained in large grains is smaller, decreasing the polarization degree of the thermal dust emission that is dominantly produced by aligned, large grains. This explains the second effect.

Figure 6 shows the polarization spectra obtained with both grain alignment and disruption by RATs (with RATD), assuming different values of tensile strength, i.e., $S_{\text{max}} = 10^7$ erg cm$^{-3}$ (left panel) and $S_{\text{max}} = 10^9$ erg cm$^{-3}$ (right panel). In the left panel, the low-$T_d$ curves are the same as those in Figure 5 (blue, orange, green, and dashed–dotted red lines). However, differing from Figure 5, the polarization degree decreases as dust temperature increases beyond a critical value (i.e., $\approx 34$ K, the dotted violet and dashed brown lines). Higher $S_{\text{max}}$ leads the disruption to occur at a higher critical dust temperature (i.e., $\approx 38$ K, the dashed brown line). The reason is that dust grains, exposed to strong radiation (indicated by where the dust temperature is high, see Figure 1(d)), can be rotated extremely fast due to strong radiative torques while damping is inefficient (because of a low gas density, Figure 1(c)), resulting in RATD as described in Section 3.2. For $T_d$ lower than the critical temperature, on the contrary, the radiative torques are weaker, and the damping process is more substantial (because gas is denser) so that the RATD cannot occur and thus the results are the same as those for the classical RATs calculations. The disruption leads to a drop in the polarization degree. The critical temperature above which RATD occurs and the level of the decline depend on the internal structure of the grains controlled by $S_{\text{max}}$. The composite grains ($S_{\text{max}} = 10^7$ erg cm$^{-3}$) are more easily disrupted, resulting in a significant decrease of the polarization.
degree (Figure 6, left panel), than for the compact grains ($S_{\text{max}} = 10^7 \text{ erg cm}^{-3}$) (Figure 6, right panel).

Figure 7 shows the polarization spectrum for the case of mixed silicate and carbon grains in which both grain populations are aligned by RATs. Similar to Figure 6, the disruption occurs for $T_d > 34$ K. In this case, the spectrum shows an increase and then a plateau feature, which differs from Figure 6. The reason is that the polarization degree is the ratio of the polarized intensity ($I_{\text{pol}}$) to the total intensity ($I_{\text{em}}$) (Equation (1)). Since the $T_d$ of silicate grains is lower than that of carbon grains, their spectrum slopes differ from each other. When only silicate grains are aligned the different spectrum slopes of $I_{\text{pol}}$ to $I_{\text{em}}$ result in a slope in polarization spectrum (see, e.g., Figure 6). When both silicate and carbon grains are aligned, $I_{\text{pol}}$ and $I_{\text{em}}$ differ by a factor of a degree of grain alignment, which results in a flat spectrum. The degree of grain alignment is defined by $f_{\text{max}}$ (Equation (12)). For a combination of carbon and silicate grains, the imperfectly aligned grains ($f_{\text{max}} < 1$) can reproduce observations (see, e.g., Draine & Fraisse 2009; Guillet et al. 2018). Grains with higher values of $f_{\text{max}}$ (right panel) produce more polarized thermal emission than those with lower values of $f_{\text{max}}$ (left panel).

Figure 8 shows the polarization degree at 89 $\mu$m (left panel) and 154 $\mu$m (right panel) with respect to dust temperature. In the case without RATD (dotted lines), the polarization degree first increases rapidly with increasing dust temperature and then slowly changes (as shown in Figure 5). Accounting for RATD, the polarization degree first increases with $T_d$ and then rapidly declines once the dust temperature exceeds a critical value, which depends on the grains’ tensile strength as shown in Figure 6. The critical dust temperature is lower for weaker grains (i.e., lower value of $S_{\text{max}}$) because of an effective disruption, which leads to a deeper decrease of the polarization degree in comparison to stronger grains.

Above, we assume that all grains have the same tensile strength ($S_{\text{max}}$). However, the tensile strength of composite grains scales with the radius of monomers as $a_p^{-2}$ (see Hoang 2019 for a detailed demonstration), which implies that large grains (comprising many monomers) are more breakable than smaller grains presumably having a compact structure. As an example, we set...
for all grains with size $a \leq 0.1 \mu m$, while we set $S_{\text{max}} = 10^6 \text{ erg cm}^{-3}$ for smaller grains. The results are shown in Figure 9, black solid lines. The trend of the polarization degree also shows an increase and decrease feature to dust temperature. However, for $T_d > T_{\text{crit}}$ (i.e., denoted by the position B), its amplitude is higher than in the case of fixed $S_{\text{max}}$. The reason is as follows. When the RATD does not occur, the polarization is higher for higher dust temperature/stronger radiation. When the dust temperature is just enough for RATD to occur, the disruption mostly affects smaller grains (i.e., low $S_{\text{max}}$). Because the dust temperature increases, the RATD can affect smaller grains (i.e., higher $S_{\text{max}}$). The reason is that the polarization follows the fixed $S_{\text{max}} = 10^6 \text{ erg cm}^{-3}$ case, as shown in Figure 8.

Figure 10 shows the polarization degree of thermal dust as a function of the grain temperature, assuming that both carbon and silicate grains are aligned. The results generally show that the polarization degree drops at the same critical dust temperature as Figure 8 in which only silicate grains are aligned. However, the mixed grain model results in higher polarization, as well as in less decline than in the case of single grains due to the contribution of aligned carbon grains. With the $T_d - n_H$ relation, we varied the value of $n_H$ by 10% but we do not see a significant change (i.e., the correlation coefficient is $\leq 0.99$). However, another relation of $n_H$ to $T_d$ could have a more significant effect.

### 4.3. Interpretation of Observations

Since the $T_{\text{crit}} \approx 30–34 \text{ K}$ critical dust temperature above which the polarized thermal dust emission drops for $S_{\text{max}} = 10^6–10^7 \text{ erg cm}^{-3}$ (see Figures 8, 10) is consistent with observations (see Figure 2), Figure 11 shows only the numerical results for $S_{\text{max}} = 10^7 \text{ erg cm}^{-3}$ with a variation of the silicate grain size distribution power index $\beta$ overlaid over the observational data. For illustration, we also show the results from the RATs model without the disruption effect (dashed line). Since RATs theory implies that stronger radiation strength causes more torques acting on grains, which results
Figure 9. Effect of the size-dependent tensile strength on the fractional polarization emission of silicate grains. The dotted blue line and the dashed orange line are computed for a fixed $S_{\text{max}}$ as in Figure 8. The solid black line is the model prediction for a size-dependent $S_{\text{max}}$ (see the text for details).

Figure 10. Same as Figure 8, but both silicate and carbon grains are assumed to be aligned with $f_{\text{max}} = 0.5$. The trend and the critical temperature are the same but the decline is less steep and the polarization amplitude is higher than in the case of silicate grains alone.

Figure 11. Comparison of the polarization degree of dust emission from our models with observations at 89 $\mu$m (left panel) and at 154 $\mu$m (right panel). Background colored points show the observational polarization degree (Figure 2). Colored lines are the models for different values of the power index $\beta$. The dashed line shows the results without RATD, while solid lines show results with RATD. Tensile strength is $S_{\text{max}} = 10^7$ erg cm$^{-3}$. Only silicate grains are aligned, and carbons are randomly oriented.
in higher polarization, then this classical RATs model can only lead to an increase of the dust polarization degree with respect to dust temperature and fails to explain its decrease beyond $T_{\text{crit}}$ dust temperature (as discussed in Section 4.2). When the rotational disruption mechanism is incorporated into RATs (solid lines), the model can reproduce the increase and decrease features from observations. For $T_d < T_{\text{crit}}$, the disruption does not proceed; hence, the model is exactly as classical RATs, which accounts for the increase of the polarization degree. For $T_d \geq T_{\text{crit}}$, on the contrary, the disruption occurs so that large grains are disrupted into many smaller fragments. The enhancement of smaller grains causes a decrease in the polarization degree at these FIR wavelengths.

Furthermore, different solid lines correspond to different values of the grain size distribution power index $\beta$. In the case of silicate grains alone, a simple $\chi^2$ calculation as in Table 1 shows that it gets minimum at $\beta \simeq -4.0$ to observational data at 89 $\mu$m, while it is slightly lower as $\beta \simeq -4.1$ to 154 $\mu$m data. Hence, the slope of the size distribution is steeper than the MRN size distribution for the standard interstellar medium (Mathis et al. 1977), which is evidence of enhancement of small grains by RATD. Note that 154 $\mu$m probes different (more embedded) layers of the $\rho$ Oph-A than the 89 $\mu$m observations do, thereby the size distribution could be slightly different. Polarimetric data at longer wavelengths (e.g., 850 $\mu$m JCMT/SCUBA-2 observations, see Kwon et al. 2018), which trace bigger grain size, are desired to get a more comprehensive picture.

Figure 12 shows the comparison for a mixture of carbon and silicate grains with respect to observations. As shown in Section 4.2, both grain size distribution ($\beta$) and degree of alignment ($f_{\text{max}}$) control the amplitude of the polarization degree, but they do not affect the spectrum trend. We found that the same range of $\beta$ as in Figure 11 also nicely fits the observational trend with $f_{\text{max}} \simeq 0.35$. In this case, the $\chi^2$ calculation in Table 1 indicates that $\beta \simeq -4.0$ and $\beta \simeq -4.1$ also result in minimum $\chi^2$ to observed data at 89 $\mu$m and 154 $\mu$m, respectively.

### 4.4. Limitations of the Model

Our model’s primary and most sensitive input parameters are the local gas column density and the local dust temperature. The first controls the damping process of the rotating grains, while the second defines the angular rotational rate of grains. The value for the gas column density is derived from a spherical model, whereas the value for the dust temperature is adopted from observations. Therefore, our results contain uncertainties, and we would like to address here the main limitations of our model. First, the adopted value of dust temperature is, in fact, the projection on the plane of the sky, the actual value could be higher than these. Second, the dust temperature and gas density maps are derived from only three FIR bands of Herschel/PACS (60, 100, and 160 $\mu$m). The derivation could be more accurate if the (sub)millimeter and radio bands are taken into account as they were in Chuss et al. (2019). However, we expect that accounting for local variations of dust temperature and gas number density could explain the observational scatter, but should not change the trend or our conclusions.

Because our main input parameters are the local values, our prescription will be easy to incorporate into more elaborate models that have better physical treatments for the gas and dust properties, such as 3D radiative dust modeling codes (e.g., Dullemond et al. 2012; Liseau et al. 2015).

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**Figure 12.** Similar to Figure 11 but for a combination of aligned carbonaceous and silicate grains. The same range of $\beta$ can match better to the observations with the degree of alignment $f_{\text{max}} = 0.35$.

**Table 1.**

| $\beta$ | $\chi^2$ (89 $\mu$m, $f_{\text{max}} = 1$) | $\chi^2$ (154 $\mu$m, $f_{\text{max}} = 0.35$) |
|---------|---------------------------------|---------------------------------|
|         | sil grain | car + sil grain | sil grain | car + sil grain |
| $-3.5$  | 4.99     | 3.41            | 10.62     | 7.40            |
| $-3.6$  | 3.45     | 2.65            | 7.60      | 5.69            |
| $-3.7$  | 2.36     | 2.03            | 5.12      | 4.15            |
| $-3.8$  | 1.68     | 1.59            | 3.25      | 2.86            |
| $-3.9$  | 1.37     | 1.35            | 1.98      | 1.89            |
| $-4.0$  | 1.34     | 1.31            | 1.26      | 1.28            |
| $-4.1$  | 1.53     | 1.44            | 1.01      | 1.02            |
| $-4.2$  | 1.86     | 1.71            | 1.09      | 1.04            |
| $-4.3$  | 2.26     | 2.08            | 1.41      | 1.28            |
| $-4.4$  | 2.71     | 2.50            | 1.84      | 1.67            |
| $-4.5$  | 3.15     | 2.94            | 2.33      | 2.12            |

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**Observations Computed by $\chi^2 = \sum (\frac{P_{\text{obs}} - P_{\text{mod}}}{\sigma})^2$ with N the Number of Data Points.**
Finally, we note that the magnetic field geometry is assumed to not vary along the line of sight toward $\rho$ Oph-A in the modeling. The effect of turbulent magnetic field would reduce the polarization degree predicted, but the trend $P(\%)$ versus $T_d$ is not affected. Nevertheless, the inferred magnetic field direction shown in Figure 2 in Santos et al. (2019) indicates the coherent magnetic stream lines in $\rho$ Oph-A. The turbulence, therefore, may occur at a very small scale.

5. Summary and Conclusions

We showed and interpreted the relation between the fractional polarization of thermal dust emission and dust temperature in the $\rho$ Oph-A molecular cloud using the archival SOFIA/HAWC+ observations at 89 and 154 $\mu$m. The observed fractional polarization first increases with increasing dust temperature and then decreases once the dust temperature exceeds $\approx 25–32$ K. This is similar to what has been seen in Planck data for other clouds (Planck Collaboration et al. 2020). This trend differs from the prediction by the classical RAT theory and represents a challenge to grain alignment theory.

We calculated the polarization degree of thermal dust emission by simultaneously considering grain alignment and rotational disruption (RATD) induced by RATs. The RATD mechanism relies on the extremely fast rotation of large grains exposed in a strong radiation field (or high dust temperature in equivalent). For sufficiently high rotation rate, the centrifugal force can exceed the binding force that holds the grain’s structure and disrupts the large grain into smaller species. Since RATs are stronger for larger grains, the RATD mechanism constrains the upper limit for grain tensile strength that holds the grain on the grain tensile strength. Therefore, may occur at a very small scale. Since RATs are stronger for larger binding force that holds the grain on the grain tensile strength

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ORCID iDs
Le Ngoc Tram & Thiem Hoang & Hyeseung Lee & Fabio P. Santos & Archanaa Soam & William T. Reach

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