Filling vacancies in a Prussian blue analogue using mechanocchemical post-synthetic modification †

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Mechanochemical grinding of polycrystalline powders of the Prussian blue analogue (PBA) Mn[Co(CN)\textsubscript{6}]\textsubscript{2/3}·\textsubscript{1/3}·H\textsubscript{2}O and K\textsubscript{5}Co(CN)\textsubscript{6} consumes the latter and chemically modifies the former. A combination of inductively-coupled plasma and X-ray powder diffraction measurements suggests the hexacyanometallate vacancy fraction in this modified PBA is reduced by approximately one third under the specific conditions we explore. We infer the mechanocchemically-driven incorporation of [Co(CN)\textsubscript{6}]\textsuperscript{3−} ions onto the initially-vacant sites, coupled with intercalation of charge-balancing K\textsuperscript{+} ions within the PBA framework cavities. Our results offer a new methodology for the synthesis of low vacancy PBAs, unlocking novel, high capacity PBA battery materials.

Prussian blue analogues (PBAs) are an important and topical family of battery materials with a number of considerable advantages over longer-established charge storage systems.\textsuperscript{10} On the one hand, they are chemically versatile, inexpensive, and easily made by aqueous precipitation from widely-available precursors. And, on the other hand, PBA electrochemistry is characterised by a combination of high specific capacity for Na\textsuperscript{+}/K\textsuperscript{+} insertion, rapid charge/discharge rates, and long cycle lives.\textsuperscript{4}

One key limitation of PBA chemistry as battery materials is the remarkably strong tendency for vacancy incorporation within the PBA structure.\textsuperscript{25} Whilst hexacyanometallate vacancies help improve structural stability and increase bulk ionic conductivity, their presence reduces specific capacity.\textsuperscript{2} Increasing energy density therefore requires synthetic routes that minimise vacancies.\textsuperscript{4}

Traditional PBA synthesis routes usually yield samples with nominal compositions M[\textit{M′}(CN)\textsubscript{6}]\textsubscript{2/3}·\textsubscript{1/3}·H\textsubscript{2}O (here M and M′ are di- and trivalent transition-metal cations, respectively, and the symbol □ represents a M′-site vacancy).\textsuperscript{5} The corresponding structure is based on the simple cubic lattice; M\textsuperscript{2+} and \textit{M′}(CN)\textsubscript{6}\textsuperscript{3−} species decorate alternate sites with one third of the hexacyanometallate sites occupied by coordinated and zeolitic water [Fig. 1(a)].\textsuperscript{5} While vacancies increase ionic conductivity\textsuperscript{2} and can even help stabilise the structure during electrochemical cycling,\textsuperscript{10} their presence limits charge capacity. From an electrochemical perspective, the ideal PBA composition is instead the non-defective system AM[\textit{M′}(CN)\textsubscript{6}] (A = monovalent alkali metal cation) because there is now scope for two separate one-electron processes—e.g. M(III)[\textit{M′}(III)(CN)\textsubscript{6}] ⇌ AM(II)[\textit{M′}(III)(CN)\textsubscript{6}] = A\textsubscript{2}M(II)[\textit{M′}(II)(CN)\textsubscript{6}]—and hence a much improved theoretical charge-storage capacity [Fig. 1(b)].\textsuperscript{11}

The two most widely-employed approaches for reducing vacancy concentrations are to bias crystallisation with large excesses of alkali cation\textsuperscript{12} and/or to employ chelating agents (e.g. citrate) to slow down precipitation kinetics.\textsuperscript{13,14} Both types of approach involve considerable precursor waste, which is an important consideration in scale-up. Moreover they have proven to be successful only for the synthesis of PBAs in their fully reduced state.\textsuperscript{12} Consequently there is strong interest in developing alternative approaches to vacancy reduction in this family.\textsuperscript{5}

Influenced by the use of mechanochemistry to allow post-synthetic metallation of a variety of porous frameworks,\textsuperscript{15,17} and also its recent application to PBA synthesis,\textsuperscript{18,20} we sought to establish whether the technique might help reduce the vacancy fraction in PBAs. Our reasoning was that the success of chelation strategies\textsuperscript{13,14} implies vacancies are largely a kinetic—rather than thermodynamic—phenomenon in PBAs, and so milling may provide an atom-efficient methodology for overcoming the kinetic barrier to ion incorporation.
We synthesised polycrystalline samples of the canonical PBA Mn[Co(CN)₆]₂/₃ · xH₂O following the approach of Ref. [5]. This particular PBA has the dual advantages of high M-site lability (high-spin d⁶ configuration of Mn²⁺)—which we expected to facilitate structural reorganisation in the solid-state—and an inert M’-site configuration (Co³⁺, low-spin d⁶) to avoid unwanted side-reactions during milling. Stoichiometric quantities of Mn[Co(CN)₆]₂/₃ · xH₂O and K₃[Co(CN)₆] were loaded within a ball-mill, and the mixture milled for up to three hours. The reaction we hoped to effect is given by the (idealised) scheme

\[
\text{Mn[Co(CN)₆]₂/₃} \rightarrow \text{KMn[Co(CN)₆]}.
\]

Small fractions of the reaction mixture were removed at successive time intervals to allow interrogation of the PBA composition as a function of milling time.

Inductively-coupled plasma (ICP) measurements of these milled samples gave the compositional variation shown in Fig. 2(a), where we plot the Co/Mn ratio \( \phi = \frac{f(\text{Co})}{f(\text{Mn})} \). Note that, in preparing our samples for ICP analysis, we removed any remaining K₃[Co(CN)₆] through washing, and digested the insoluble PBA in a nitric acid solution. Our focus is on Mn and Co compositions, since ICP analysis of K content is notoriously unreliable. We infer K content on the basis of charge-balance. For the as-prepared sample, \( \phi = 0.700(17) \), which suggests the initial composition was K₀.₆₇Mn[Co(CN)₆]₀.₃₃O.₃₀ · xH₂O. Milling increases the value of \( \phi \) such that after three hours \( \phi = 0.80(3) \); the PBA composition is now K₀.₆₀Mn[Co(CN)₆]₀.₃₀O₂.₂₀ · xH₂O. The evolution of \( \phi \) with milling time \( t \) is well fit by the simple expression

\[
\phi(t) = \left[ \frac{f(\text{Co})}{f(\text{Mn})} \right]_t = \phi_\infty + \left( \phi_0 - \phi_\infty \right) \exp(-t/\tau),
\]

with empirical parameters \( \phi_0 = 0.71, \phi_\infty = 0.80, \tau = 43 \text{ min} \). Consequently our data suggest that, under the specific milling conditions we explore, approximately one third of the vacancies can be filled mechanochemically with a filling half-life of about 30 minutes (= \( \tau \ln 2 \)).

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Fig. 1 Representative (a) defective and (b) non-defective PBA structures illustrated for the nominal compositions Mn[Co(CN)₆]₂/₃ and KMn[Co(CN)₆]. Mn and Co coordination polyhedra are shown in translucent pink and blue, respectively; K, C and N atoms in green, black and dark blue; coordinated water molecules shown as white spheres. Zeolitic water is omitted for clarity.

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Fig. 2 Evidence for mechanochemical vacancy filling in Mn[Co(CN)₆]₂/₃. (a) Variation in Co/Mn ratio with milling time as determined using ICP. The bold line shows the fit to data obtained using Eq. (1); the fine grey line is the corresponding fit when all data sets are included. (b) PXRD traces (black lines) and fits (coloured lines) for milled samples; successive curves are shifted vertically by a constant amount. Three reflections associated with K₃[Co(CN)₆] are marked with an asterisk. (c) Phase fractions and intensity ratios extracted from (b) as discussed in the text. The bold lines show the fit-to-data using Eq. (1).

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Powder X-ray diffraction (PXRD) measurements also support this interpretation. We carried out a new set of milling experiments under identical conditions but focussing on the initial 80 minutes. Again we extracted small fractions of the reaction mixture throughout milling at intervals of 10 minutes up to one hour,
and after 80 minutes. The PXRD patterns collected for these fractions (Cu Kα radiation) evolved smoothly as a function of milling time [Fig. 2(b)]. In particular, we observed a monotonic decrease in the intensities of reflections associated with K₃[Co(CN)₆]₃. In order to quantify this point we carried out a combination of Pawley and Rietveld refinements. We used the former to model the PBA component (so as not to presume its composition) and the latter for K₃[Co(CN)₆]₃ (and an Al₂O₃ standard); full details are given as SI, including discussion of our treatment of preferred orientation effects and of peak broadening. By fixing the relative intensities assigned to the PBA reflections we refined a corresponding phase scale factor \( f_{\text{PBA}} \) for each data set. The evolution of the relative \( K₃[Co(CN)₆]₃ \) fraction \( f_K \) is then given by

\[
f_K(t) = \frac{x_K(t)}{x₀} \cdot \frac{f_{\text{PBA}}(0)}{f_{\text{PBA}}(t)},
\]

where \( x_K(t) \) is the Rietveld-refined phase fraction of K₃[Co(CN)₆]₃ at milling-time \( t \). Our results are shown in the left-hand panel of Fig. 2(c). These indicate that approximately 45% of the K₃[Co(CN)₆]₃ component is consumed during milling, which is in good agreement with the ICP results.

But there is direct evidence too from PXRD reflection intensities of incorporation of \( K^+ \) and \( [Co(CN)₆]^{3-} \) within the PBA structure. The ratio

\[
\alpha = \sqrt{I(400)/I(200)}
\]

varies approximately linearly with the degree of vacancy filling and \( K^+ \) intercalation. Full details are given as SI, but on an intuitive level the (400) reflection is sensitive to density modulations with wavelength \( \lambda(400) = a/4 \) for the PBA structure projected onto the cube axis, and the (200) to modulations with wavelength \( \lambda(200) = a/2 \). Intercalation of \( K^+ \) ions within the PBA cavities \( (x,y,z \in \{1/2, 0, 1/2\}) \) increases the strength of the former type relative to that of the latter. Fixing the PBA scale factors \( f_{\text{PBA}} \) as above and allowing the reflection intensities to refine, we can determine the experimental variation in \( \alpha \) with milling time [right-hand panel of Fig. 2(c)]. While the uncertainty in \( \alpha \) is not small, we nonetheless observe the expected trend: namely, that its value increases with milling time, consistent with intercalation of \( K^+ \). For completeness, we note that we also notice a systematic variation in PBA lattice parameter accompanying intercalation (see SI for further discussion).

Taking together our ICP and PXRD results, we carried out a collective empirical fit of all our data using the functional form of Eq. (1) with a common characteristic time-scale \( \tau \). These collective fits are shown in Fig. 2(a,c); their consistency implies that the observed trends in chemical composition, phase fractions, and diffraction intensities arise from a single common process. Hence we conclude there is evidence for mechanochemical insertion of K₃[Co(CN)₆]₃ into this PBA, that involves simultaneous filling of hexacyanometallate vacancies and intercalation of \( K^+ \) cations.

Of course our analysis does not shed light on the mechanism of this filling process. That—under the conditions we study here—the limiting fraction of vacancies is non-zero suggests an inhomogeneous distribution of filled vacancies in the PBA component of our mixture. A reasonable hypothesis is that hexacyanometallate migration in the solid-state is itself facilitated by \( M^\prime \)-site vacancies, such that filling inhibits further reaction. In such a scenario, one expects the interior of PBA particles to remain defective as their surfaces react. With this in mind, increasing milling rate may allow a reduction in particle size that in turn translates to higher filling fractions. Our very preliminary measurements have at least found that reducing milling rate does indeed reduce both peak broadening and vacancy filling—and so this is an obvious avenue for further investigation. Likewise we cannot yet say definitively whether hexacyanometallate anion incorporation is limited to the \( M^\prime \) site, or whether intercalation on the \( A \)-site is also possible, such as has been observed for complex ions in the related thiocyanate PBAs.

In the context of optimising PBA-based battery materials a number of obvious follow-up experiments must now be carried out. First, it is important to show that vacancy filling in redox-active PBAs is possible (our own preliminary study of Mn[Fe(CN)₆]₁/₃ suggests it is). Second, the vacancy filling fraction should be maximised by varying milling rate, exploiting ion and liquid assisted grinding approaches and/or pre-milling reagents. And, third, the crucial link to electrochemical performance remains to be made. Other variations on the theme may also be possible, such as milling with varying \( A_3[MCN]_6 \) salts to generate multivariate PBA. Our key result here, of course, has been to demonstrate that post-synthetic control over vacancy fraction is at least possible in PBAs using a mechanochemical approach. The exploitation of mechanochemistry in post-synthetic modification of this type remains somewhat under-explored, and a broader implication of our work is that similar control over vacancy fractions in other porous materials (e.g. metal–organic frameworks) may now be possible.

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Conflict of interest

There are no conflicts to declare.

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