DISCOVERY OF A VISUAL T-DWARF TRIPLE SYSTEM AND BINARITY AT THE L/T TRANSITION

Jacqueline Radigan$^{1,2}$, Ray Jayawardhana$^2$, David Lafrenière$^1$, Trent J. Dupuy$^{4,7}$, Michael C. Liu$^5$, and Alexander Scholz$^6$

1 Space Telescope Science Institute, 3700 San Martin Drive, Baltimore, MD 21218, USA; radigan@stsci.edu
2 Department of Astronomy and Astrophysics, University of Toronto, 50 St. George Street, Toronto, ON M5S 3H4, Canada
3 Département de Physique, Université de Montréal, C.P. 6128 Succ. Centre-Ville, Montréal, QC H3C 3J7, Canada
4 Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, Cambridge, MA 02138, USA
5 Institute for Astronomy, University of Hawaii, 2680 Woodlawn Drive, Honolulu, HI 96822, USA
6 School of Physics and Astronomy, University of St Andrews, North Haugh, St Andrews, KY169SS, UK

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ABSTRACT

We present new high contrast imaging of eight L/T transition brown dwarfs (BDs) using the NIRC2 camera on the Keck II telescope. One of our targets, the T3.5 dwarf 2MASS J08381155+1511155, was resolved into a hierarchal triple with projected separations of 2.5 ± 0.5 AU and 27 ± 5 AU for the BC and A(BC) components, respectively. Resolved OSIRIS spectroscopy of the A(BC) components confirms that all system members are T dwarfs. The system therefore constitutes the first triple T-dwarf system ever reported. Using resolved photometry to model the integrated-light spectrum, we infer spectral types of T3 ± 1, T3 ± 1, and T4.5 ± 1 for the A, B, and C components, respectively. The uniformly brighter primary has a bluer $J−K_s$ color than the next faintest component, which may reflect a sensitive dependence of the L/T transition temperature on gravity, or alternatively divergent cloud properties among components. Relying on empirical trends and evolutionary models we infer a total system mass of 0.034–0.104 $M_\odot$ for the BC components at ages of 0.3–3 Gyr, which would imply a period of 12–21 yr assuming the system semimajor axis to be similar to its projection. We also infer differences in effective temperatures and surface gravities between components of no more than $\sim$150 K and $\sim$0.1 dex. Given the similar physical properties of the components, the 2MA0838+15 system provides a controlled sample for constraining the relative roles of effective temperature, surface gravity, and dust clouds in the poorly understood L/T transition regime. For an age of 3 Gyr we estimate a binding energy of $\sim$9 $\times$ 10$^{41}$ erg for the wide A(BC) pair, which falls above the empirical minimum found for typical BD binaries, and suggests that the system may have been able to survive a dynamical ejection during formation. Combining our imaging survey results with previous work we find an observed binary fraction of 4/18 or 22$^{+10}$% for unresolved spectral types of L9–T4 at separations $\gtrsim 0\prime.1$. This translates into a volume-corrected frequency of 13$^{+7}$%–18 or 22$^{+10}$% reported outside the transition. Our reported L/T transition binary fraction is roughly twice as large as the binary fraction of an equivalent L9–T4 sample selected from primary rather than unresolved spectral types (6$^{+6}$%); however, this increase is not yet statistically significant and a larger sample is required to settle the issue.

Key words: binaries: visual – brown dwarfs – stars: individual (2MASS J08381155+1511155)

Online-only material: color figures

1. INTRODUCTION

The L/T transition, roughly spanning L8–T5 spectral types, is characterized by dramatic spectral evolution at near-infrared wavelengths at a near-constant effective temperature of $\sim$1200 K (Golimowski et al. 2004; Stephens et al. 2009). Rather than following a sequence in effective temperature, evolution across the L/T transition follows the disappearance of condensate clouds from brown dwarf (BD) photospheres as progressively larger dust grains gravitationally settle faster than they can be replenished (e.g., Ackerman & Marley 2001; Tsuji 2002; Marley et al. 2002; Allard et al. 2003; Woitke & Helling 2003). As condensate opacity declines, the average $\tau=2/3$ surface moves to deeper, warmer atmospheric layers. This effect is seen most clearly at wavelengths of $\sim$1 $\mu$m ($Y$ and $J$ bands) for which clouds are a dominant opacity source. From L8–T5 spectral types the $\sim$1 $\mu$m flux increases by a factor as high as $\sim$2.5 (“$J$-band brightening”; Dahn et al. 2002; Tinney et al. 2003; Vrba et al. 2004; Dupuy & Liu 2012; Faherty et al. 2012) as the dust opacity declines. The observed constancy in effective temperature across the L/T transition results from a coincidence of opposing phenomena: cooling of the atmosphere is roughly offset by its increasing transparency to deeper layers (Saumon & Marley 2008). The processes governing the dissipation and settling of condensates across the L/T transition remain poorly understood, with models generally predicting a more gradual change in cloud properties over a wider range of effective temperatures than is observed (e.g., Tsuji & Nakajima 2003; Marley et al. 2002; Allard et al. 2003). It is debated as to what extent the rapid decrease in cloud opacity is due to global changes in cloud thickness and position, changing grain properties, increasing rates of grain sedimentation, or a decreasing cloud filling fraction over the BD surface (e.g., Burrows et al. 2006; Saumon & Marley 2008; Burgasser et al. 2002). Recent observa-

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Multiple systems have already played an important role in testing formation, atmosphere, and evolutionary models for very low mass (VLM, testing formation, atmosphere, and evolutionary models for very small objects (e.g., Liu et al. 2006; Stassun et al. 2007; Burgasser et al. 2007; Dupuy & Liu 2012). When attempting to understand the L/T transition, multiple systems are important in two major ways. First, it has been suggested that there could be an unusually high binary fraction in this regime (∼L9−T4 spectral types). According to a population synthesis of Burgasser (2007), this hypothesized increase reflects a dip in the luminosity function of bona fide single BDs at these spectral types (e.g., due to rapid evolution through this regime), in contrast to a roughly constant luminosity function for unresolved binaries whose integrated-light spectral types mimic those of true transition objects. Thus multiplicity searches at the L/T transition are important in order to determine the degree of binary contamination, and to identify contaminants. Second, if L/T transition binaries are resolved into constituent parts or straddling the L/T transition, they can provide strong tests of models where two free parameters, the age and metallicity of the system, are fixed. For instance, the identification of “flux-reversal” binaries wherein the secondary component is brighter than the primary in the J band has provided direct evidence that this brightening is a real evolutionary feature associated with the disappearance of dust clouds (e.g., Liu et al. 2006; Looper et al. 2008). Furthermore, in cases where masses can be constrained from visual orbits, these systems can act as gravity benchmarks which will further our understanding of the dependence of cloud properties on surface gravity.

Here we present high contrast imaging observations of eight BDs occupying the sparsely populated L/T transition, designed to search for hitherto undetected multiples. One object, the T3.5 dwarf 2MASS J08381155+1511155 (2M0838+15 hereafter), was resolved into a triple system. This discovery constitutes the first triple T-dwarf ever reported. In Section 2 we describe our target sample including the discovery of 2M0838+15, our observations, and data reduction. In Section 3 we analyze the resolved NIRC2 images and OSIRIS spectroscopy of the newly resolved 2M0838+15 system. In Section 4 we describe the search for companions and detection limits around our entire sample. In Section 5 we combine our results with those from previous surveys to infer a binary fraction for L9−T4 spectral types, and to test whether there is a statistically significant increase in binary frequencies inside the L/T transition. In Section 6 we summarize our major findings and discuss our results in the context of the L/T transition and substellar formation models.

2. OBSERVATIONS AND DATA REDUCTION

Here we present high contrast imaging observations of eight L/T transition BDs using the NIRC2 camera on the Keck telescope obtained on the night of 2010 January 8. One target in our sample was resolved into a triple system, for which we obtained follow-up imaging with NIRC2 on 2010 March 22 and partially resolved spectroscopy using OSIRIS on 2011 December 3. These three data sets are described in the following subsections.

2.1. Target Selection

Details for our NIRC2 imaging targets are provided in Table 1. The targets were selected to overlap with an L/T transition sample of BDs targeted for variability monitoring (Radigan et al. 2011) where possible, while gaps in our program were filled by additional targets with late-L and T spectral types that were observable at low air mass at the time of our observations. Objects were further culled based on not having previously been targeted by a high resolution imaging survey, and possessing a suitable tip-tilt (TT) star within 50′. One object fulfilling these criteria was an unpublished T-dwarf, 2M0838+15, whose discovery and spectral confirmation is described in the following subsection.

2.1.1. Discovery and Spectral Confirmation of 2M0838+15

The early T-dwarf 2M0838+15 was discovered in 2008 from our own proper motion cross-match of Two Micron All Sky Survey (2MASS) and Sloan Digital Sky Survey (SDSS) catalogs (described in Radigan et al. 2008), but remained unreported. This source was independently discovered as a T-dwarf candidate in a cross-match of 2MASS and WISE by Aberasturi et al. (2011).

We obtained spectral confirmation for 2M0838+15 on 2008 March 1 using the SpeX Medium-Resolution Spectrograph (Rayner et al. 2003) at NASA’s Infrared Telescope Facility (IRTF). Observations were made in the short slit (15′′) prism mode (0.8−2.5 μm), with a 0.5′′ wide slit. The seeing was 0.8′′−0.9′′. We obtained ten 180 s exposures consisting of five AB pairs with a nod step of 7′′ along the slit. For telluric and instrumental transmission correction the A0V star HD 79108 was observed immediately after the target at a similar air mass. Flat-fielding, background subtraction, spectrum extraction, wavelength calibration, and telluric correction were done using SpeXtool (Cushing et al. 2004;Vacca et al. 2003).

The unresolved spectrum for 2M0838+15 is presented in Figure 1. Based on least squares fitting of spectral templates
of the SpeX Prism Library to our data we derive a spectral type T3.5 ± 0.5 for the unresolved source.

Due to its status as an L/T transition object without previously reported high contrast imaging observations, 2M0838+15 was included in our laser guide star adaptive optics (AO) mini-survey of L/T transition BDs, described above in Section 4. Images obtained using the NIRC2 camera during the observations of 2010 January 8 revealed this source to be a hierarchal triple (Figure 2) consisting of a widely separated A(BC) pair (∼0′′5), with the BC component being further resolved into a tight double (∼0′′05).

2.2. **NIRC2 Observations of L/T Transition Dwarfs**

Observations of eight L/T transition BDs (see Table 1) were obtained in the first half of the night of 2010 January 8 using the NIRC2 narrow camera on the Keck II telescope. Due to the lack of bright natural guide stars within 20′ of our targets, the laser guide star and an off axis TT star were used for AO corrections. For each target we obtained three or more dithered images in the K_s band. We used a three-point dither pattern, offsetting targets ±2′′5 from the center of the array in both x- and y-directions, excluding the bottom-left quadrant of the array which is significantly noisier than the others. The median FWHM and Strehl ratios achieved in the K_s band were 0′′075 and 0.19, respectively. Some targets were also observed in the J and H bands but with lower image quality. Here, we only present multi-band data for the lone target in our sample that was resolved into a multiple system. Details pertaining to observations of individual targets including air mass, exposure times, number of exposures, average FWHM and Strehl ratios, and TT star magnitudes and separations are provided in Table 2.

For calibration purposes 10–15 dome flat fields (with the lamp on and off) for each bandpass were taken before sunset. Dark frames were obtained the afternoon after the observations for all but the longest exposure times (180 s and 210 s). For exposure times without corresponding dark frames the longest exposure (120 s) dark frames were simply scaled by integration time. The dark frames for each exposure time were median combined to form master dark frames for each exposure time. A master dark of the appropriate exposure time was then subtracted from all other science images. The flat field frames for a given filter were median combined and the resultant lamp-off frames subtracted from the lamp-on frames to obtain a single high signal to noise flat field for each filter. All sciences images were divided by the flat field to correct for pixel-to-pixel variations in quantum efficiency. For each science image of a given target in a given bandpass a sky frame was obtained by averaging together all other exposures wherein the target did not fall in the same quadrant of the array. The iterative (3σ clipped) median of each sky frame was scaled to match the iterative median of the corresponding science frame in the target quadrant. The scaled sky frames were then subtracted from the science frames. A bad pixel mask was constructed by identifying hot pixels in the dark frames and dead pixels in the flat field frames. Additional bad pixels missed by this method were manually flagged. Bad pixels located more than two FWHMs away from the target were corrected by replacing their value with that of a 5 × 5 pixel median filtered image. Bad pixels falling within two FWHMs of the target were interpolated using a second order surface interpolation of neighboring pixels. All pixel interpolations in the vicinity of our targets were also examined by eye. In addition to retaining the reduced individual exposures, all science images for a given filter and target were positionally cross-correlated against one another to determine relative sub-pixel offsets, interpolated onto a common grid, and stacked. Individual exposures with the narrowest FWHMs were used to search for close companions as described in Section 4, while the stacked images were used to place limits on the presence of well-separated faint companions.

Reduced images of our targets are shown in Figure 3. One of eight targets, the T3.5 dwarf 2M0838+15, was resolved into a multiple system. Images obtained revealed this source to be a hierarchal triple consisting of a widely separated A(BC) pair.

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**Figure 1.** Unresolved JHK spectrum of the 2M0838+15ABC system (black line), obtained using SpeX at the IRTF. The best-fitting template from the SpeX Prism Library, the T3.5 dwarf SDSSp J175032.96+175903.9 (Geballe et al. 2002; Burgasser et al. 2006), is over plotted as a spectral type reference (red). The next best-fitting template, the T3 dwarf SDSS J120602.51+281328.7 (Chiu et al. 2006), is also shown. The camera position angle on the sky is 45°7.

(A color version of this figure is available in the online journal.)

**Figure 2.** Reduced NIRC2 images in the J, H, and K_s bands (from left to right) of the 2M0838+15ABC system.

(A color version of this figure is available in the online journal.)
Figure 3. Postage stamps (\(K_s\) band) of all targets observed with NIRC2. In several cases the PSF is elongated in the direction of the TT star. Only a single target, 2M0838+15, was resolved into a multiple system (bottom right). The camera position angle on the sky is 45\(^{\circ}\). The PSF FWHM is indicated in brackets. (A color version of this figure is available in the online journal.)

Table 2

| Target      | SpT | Filter | \(N_{\text{exp}}\) | \(t_{\text{exp}}\) (s) | Air mass\(^a\) | FWHM (\(\arcsec\)) | Strehl | TT R Mag\(^b\) | TT Sep\(^c\) |
|-------------|-----|--------|---------------------|------------------------|----------------|---------------------|--------|---------------|-------------|
| 2M0119+24   | T2  | \(K_s\) | 3                   | 120                    | 0.065           | 0.23                | 16.0   | 9.0           |
| 2M0247+16   | T2  | \(K_s\) | 5                   | 80                     | 0.073           | 0.19                | 13.8   | 45.7          |
| 2M0328+32   | L8  | \(K_s\) | 6                   | 100                    | 0.103           | 0.085               | 16.9   | 61.2          |
| 2M0351+48   | T1  | \(K_s\) | 5                   | 80                     | 0.116           | 0.087               | 16.0   | 50.9          |
| 2M0602+40   | T5  | \(K_s\) | 2                   | 80                     | 0.111           | 0.075               | 15.9   | 40.9          |
| 2M0742+20   | T5  | \(K_s\) | 3                   | 60                     | 0.118           | 0.081               | 12.6   | 51.1          |
| 2M0758+32   | T2  | \(K_s\) | 4                   | 120                    | 0.130           | 0.081               | 12.6   | 51.1          |
| 2M0815+13   | T3.5| \(H\)  | 4                   | 210                    | 0.130           | 0.081               | 12.6   | 51.1          |

Notes:
\(^a\) Air mass at the start of the observation.
\(^b\) R magnitude of the tip-tilt star.
\(^c\) Angular distance between the target and tip-tilt star.

(\(\sim0.5\)) scale which provided a slightly larger field of view and increased efficiency by allowing us to dither on-chip rather than requiring separate blank sky frames. We obtained two AB pairs of spectra in the \(H\) band with 15 minute and 5 minute exposures, respectively, and one AB pair of \(K\)-band spectra with 6 minute exposures.

We observed the A0V star HD 64586 and a probable K giant star BD+211974 for telluric correction before (\(H\) band only) and after (\(H\) and \(K\) bands) the science observations, at similar air mass. Due to bad weather and initial problems acquiring the science target, observations of the first telluric occurred over 2 hr ahead of the science exposures. Unfortunately although our second telluric BD+211974 is listed in SIMBAD as an A0V star, we discovered upon obtaining a spectrum that it is more likely an M or K giant with strong CO absorption features in the \(K\) band (although relatively featureless in \(H\)). In order to use BD+211974 for telluric correction, knowledge of its intrinsic spectrum is required. To this end we obtained a spectrum of BD+211974 using SpeX at the IRTF in short wavelength cross dispersed mode on 2012 June 9, using the A0V star HD79108 for telluric correction. The spectrum was reduced using SpeXtool (Cushing et al. 2004; Vacca et al. 2003).

2.3. OSIRIS Spectroscopy of the 2M0838+15 System

Spatially resolved spectra of the 2M0838+15 components were obtained on 2011 December 3 in the latter half of the night using the OSIRIS integral field unit (Larkin et al. 2006) on the Keck II telescope. Conditions were partially cloudy. The extinction only dropped below 1 mag, permitting operation of the laser, in the latter quarter of the night. The star USNO-A2.0 050−05806001, located 51\(\arcsec\)1 away, was used for TT corrections, and fell in a non-vignetted region of the guide camera field of view when the 2M0838+15 A(BC) system was aligned along the long axis of the OSIRIS spectrograph (a position angle of 19\(^{\circ}\) on the sky). We had originally planned to use the finest 0.01\(\arcsec\) plate scale and obtain blank sky frames for sky subtraction. However, because of time lost due to clouds in the first half of our run, we instead opted to use the 0.035\(\arcsec\) pixel\(^{-1}\) scale which provided a slightly larger field of view and increased efficiency by allowing us to dither on-chip rather than requiring separate blank sky frames. We obtained two AB pairs of spectra in the \(H\) band with 15 minute and 5 minute exposures, respectively, and one AB pair of \(K\)-band spectra with 6 minute exposures.

We observed the A0V star HD 64586 and a probable K giant star BD+211974 for telluric correction before (\(H\) band only) and after (\(H\) and \(K\) bands) the science observations, at similar air mass. Due to bad weather and initial problems acquiring the science target, observations of the first telluric occurred over 2 hr ahead of the science exposures. Unfortunately although our second telluric BD+211974 is listed in SIMBAD as an A0V star, we discovered upon obtaining a spectrum that it is more likely an M or K giant with strong CO absorption features in the \(K\) band (although relatively featureless in \(H\)). In order to use BD+211974 for telluric correction, knowledge of its intrinsic spectrum is required. To this end we obtained a spectrum of BD+211974 using SpeX at the IRTF in short wavelength cross dispersed mode on 2012 June 9, using the A0V star HD79108 for telluric correction. The spectrum was reduced using SpeXtool (Cushing et al. 2004; Vacca et al. 2003).
The raw spectra were sky subtracted in AB pairs, wavelength calibrated, and converted into three-dimensional data cubes (two spatial directions plus wavelength) using the OSIRIS data reduction pipeline (DRP) with the latest rectification matrices available (2010 July). The pipeline also corrects for bias variations between detector output channels, crosstalk, and electronic glitches, and attempts cosmic ray removal. One-dimensional spectra were extracted from the reduced data cubes via aperture photometry on the individual wavelength slices. A circular aperture of 2.5 pixel radius centered on each of the A and BC components was used. Residual sky levels were measured in annuli of 6 and 9 pixel inner and outer radii. Extraction of the brighter standard star spectra were conducted using a larger 4 pixel radius aperture, and residual sky levels were found to be negligible. For the A0V star HD 64586 we used the XtellCorr software package described in Vacca et al. (2003) to obtain our telluric spectrum (including scaled hydrogen line removal, and division of the spectrum by a Vega template). For the giant star BD+211974 we determined a telluric correction by dividing our non-corrected OSIRIS spectrum of BD+211974 by the fully corrected (i.e., intrinsic) SpeX spectrum. In the K band BD+211974 is our only option for telluric correction, while in the H band both HD 64586 and BD+211974 were available. When applied to the H-band science data, we found that the latter provided a slightly cleaner correction and was thus adopted in our final reduction. We verified the DRP wavelength solution by comparing a sky spectrum to a database of OH lines and found it to be good to within \( \sim 10 \AA \), which is more than sufficient for our purposes.

The resultant H and K spectra for the A and BC components, in units of relative \( F_\lambda \), are shown in Figure 4. Relative scaling of the A and BC contributions was achieved using our resolved NIRC2 photometry, while scaling between H and K bands was determined using our IRTF spectrum of the unresolved 2M0838+15 system. The final spectra are sampled with two bins per resolution element at a native resolution of \( R \sim 3800 \), but have been binned (using an error-weighted mean) by a factor of 7 to increase the signal to noise. The K-band spectrum of component A has a very low signal to noise and we were unable to extract a clean spectrum free of systematic wiggles. Thus we only show a rough spectral energy distribution for this component, in 0.03 \( \mu \)m bins. For reference we have overplotted the unresolved IRTF spectrum, and find it is reasonably well reproduced by the A+BC OSIRIS spectra. Our OSIRIS spectroscopy confirms that both the A and BC components have T spectral types (discussed further in Section 3.3.2). Given the near equal luminosity and colors of the BC components, this result confirms that all three constituents of the 2M0838+15 system are T-dwarfs.

3. 2M0838 + 15 ABC: DISCOVERY OF A VISUAL TRIPLE T-DWARF SYSTEM

3.1. Analysis of the NIRC2 Images: Binary System Properties and Component Fluxes

Binary parameters for the tight BC components were determined by fitting a double point-spread-function (PSF) model (using component A as a single PSF reference) to the data. We modeled component A as a sum of two-dimensional Gaussians,

\[
M_A(x, y) = \sum_{k=0}^{N} A_k e^{u_k} + p_0 + p_1 x + p_2 y, \tag{1}
\]

where

\[
u_k = \left( \frac{(x-x_k)\cos \theta_k}{\sigma_{k,1}} - \frac{(y-y_k)\sin \theta_k}{\sigma_{k,1}} \right)^2 + \left( \frac{(x-x_k)\sin \theta_k}{\sigma_{k,2}} + \frac{(y-y_k)\cos \theta_k}{\sigma_{k,2}} \right)^2. \tag{2}\]

Above, \( x \) and \( y \) are pixel coordinates, \( x_k, y_k, A_k, \sigma_{k,1}, \) and \( \sigma_{k,2} \) are parameters describing the position, amplitude, and widths of the \( k \)th Gaussian along major and minor axes, \( \theta_k \) is a rotation of the \( k \)th Gaussian with respect to the pixel coordinate system, and parameters \( p_0, p_1, \) and \( p_2 \) define a background plane. The fit is constrained to disallow high frequency features by requiring that \( \sigma_{k,1} \) and \( \sigma_{k,2} > 2.12 \) pixels (FWHM > 5 pixels). Our model of the single PSF then consists of 6\( N_e + 3 \) parameters where \( N_e \) is the number of Gaussian components. For each image we fit our multiple Gaussian model to component A using a Levenberg–Marquardt least-squares minimization as implemented in the IDL software MPFIT (Markwardt 2009). The fit was performed within a 39 pixel box centered on source. We fit models with \( N_e \) ranging from 1 to 9 to each image, and selected a final value of \( N_e \) that minimizes the Bayesian Information Criterion (BIC; Liddle 2007), where here BIC = \( \chi^2 + (6N_e + 3) \ln N_{\text{pix}} \), where \( N_{\text{pix}} \) is the number of data points. Next, we fit a double version of our single PSF model to the BC components, consisting of nine parameters: two specifying the pixel position of component B relative to component A, \( x_B \) and \( y_B \); two specifying the angular separation and position angle of component C from component B, \( \rho_{BC} \) and \( \theta_{BC} \); two specifying the fluxes or amplitudes of the B and C components with respect to component A, \( F_B / F_A \) and \( F_C / F_A \); and three parameters defining a plane \( c_0 + c_1 x + c_2 y \) to allow for a sloping background. Fitting was performed in a 27 pixel box centered on components BC using MPFIT. We adopted the NIRC2 plate scale of \( 0\prime\prime 009963 \) pixel\(^{-1} \) and \( 0\prime\prime 13 \) offset in position angle found by Ghez et al. (2008) in order to convert pixel coordinates to angular separations and position angles. The images were not corrected for distortion before fitting. Based on distortion corrections

\[8\] We find that up to seven components are needed to account for substructures in the PSF that are above the noise floor.

Figure 4. Resolved H and Ks spectra of the A (blue line) and BC (red line) components obtained using the OSIRIS spectrograph on the Keck II telescope. The sum of the A and BC contributions is plotted as a black line. The unresolved SpeX spectrum is shown for reference in gray and was used to scale the relative H and K contributions. (A color version of this figure is available in the online journal.)
provided by Yelda et al. (2010) the differential distortion at distances similar to the BC component separation is ~0.2 mas, and across our entire fitting box is <1 mas.

We fit our model for the A and BC components to each individual exposure taken in the J, H, and K_s bands. An example of the data, model, and residuals for a single image is shown in Figure 5. In most cases subtraction of the best-fitting model from the data leaves no significant residuals.

![Figure 5](Image)

Table 3

| Filter | No. | FWHM | Strehl | Sep (mas) | P.A. (deg) | F_B/F_A | F_C/F_A | χ^2/dof | N_b | χ^2/dof | BIC |
|--------|-----|------|--------|-----------|------------|---------|---------|---------|-----|---------|-----|
| J      | 1   | 112  | 0.032  | 48.1 ± 0.8 | -14 ± 1    | 0.60 ± 0.03 | 0.75 ± 0.03 | 1.68 | 5 | 1.84 | 2987 |
| J      | 2   | 81   | 0.061  | 49.8 ± 0.5 | -2 ± 1     | 0.63 ± 0.01 | 0.73 ± 0.01 | 1.25 | 5 | 1.62 | 2652 |
| J      | 3   | 109  | 0.041  | 48.5 ± 0.7 | -9 ± 1     | 0.61 ± 0.02 | 0.76 ± 0.02 | 1.24 | 7 | 1.59 | 2517 |
| Mean   |     |      |        | 49.1 ± 0.6 | -7 ± 1     | 0.62 ± 0.02 | 0.74 ± 0.01 |        |    |        |     |
| SD     |     |      |        | 0.9 ± 0.2 |           | 0.02 ± 0.01 | 0.01 ± 0.01 |        |    |        |     |
| H      | 1   | 98   | 0.096  | 49.7 ± 0.4 | -9 ± 1     | 0.77 ± 0.01 | 0.62 ± 0.01 | 1.15 | 5 | 1.24 | 2081 |
| H      | 2   | 86   | 0.129  | 50.8 ± 0.3 | -4 ± 1     | 0.75 ± 0.01 | 0.63 ± 0.01 | 1.11 | 6 | 0.94 | 1677 |
| H      | 3   | 80   | 0.123  | 50.2 ± 0.2 | -5 ± 1     | 0.73 ± 0.01 | 0.66 ± 0.01 | 1.15 | 5 | 1.09 | 1861 |
| H      | 4   | 67   | 0.172  | 50.1 ± 0.2 | -6 ± 1     | 0.74 ± 0.01 | 0.64 ± 0.01 | 1.11 | 7 | 1.20 | 2100 |
| H      | 5   | 73   | 0.146  | 50.0 ± 0.3 | -6 ± 1     | 0.71 ± 0.01 | 0.65 ± 0.01 | 1.21 | 7 | 1.20 | 2078 |
| H      | 6   | 95   | 0.095  | 49.7 ± 0.4 | -8 ± 1     | 0.73 ± 0.01 | 0.69 ± 0.01 | 0.93 | 4 | 1.16 | 1927 |
| Mean   |     |      |        | 50.2 ± 0.6 | -6 ± 1     | 0.74 ± 0.01 | 0.65 ± 0.01 |        |    |        |     |
| SD     |     |      |        | 0.4 ± 0.2 |           | 0.02 ± 0.01 | 0.02 ± 0.01 |        |    |        |     |
| K_s    | 1   | 89   | 0.213  | 50.1 ± 0.6 | -6 ± 2     | 0.71 ± 0.02 | 0.63 ± 0.02 | 1.17 | 3 | 0.99 | 1645 |
| K_s    | 2   | 85   | 0.245  | 50.8 ± 0.5 | -1 ± 1     | 0.71 ± 0.01 | 0.59 ± 0.01 | 0.69 | 3 | 0.71 | 1213 |
| K_s    | 3   | 74   | 0.302  | 50.8 ± 0.4 | -7 ± 1     | 0.75 ± 0.01 | 0.59 ± 0.01 | 0.84 | 4 | 0.75 | 1324 |
| K_s    | 4   | 77   | 0.253  | 51.2 ± 0.5 | -5 ± 1     | 0.73 ± 0.01 | 0.61 ± 0.01 | 0.83 | 3 | 0.72 | 1230 |
| Mean   |     |      |        | 50.9 ± 0.5 | -5 ± 1     | 0.73 ± 0.01 | 0.60 ± 0.01 |        |    |        |     |
| SD     |     |      |        | 0.5 ± 0.2 |           | 0.02 ± 0.01 | 0.02 ± 0.01 |        |    |        |     |

Notes. The weighted means and standard deviations of individual measurements in a given column are shown in bold.

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the A and BC components have identical spectral types within the system were obtained in the H and CH$_4$S (off-methane) filters using the NIRC2 narrow camera. Observing conditions were partially cloudy, the image FWHM was large ($\pm 13\arcsec$). From fitting Gaussian PSFs to these data, relative positions and fluxes were determined between the A(BC) components. We found the ($\rho_{AB}$) magnitudes between components, $\Delta J$, $\Delta H$, and $\Delta K_s$ in Table 5.

3.3. System and Component Properties Inferred from Empirical Trends and Evolutionary Models

3.3.1. Magnitudes and Colors

We used relative fluxes measured from our model fitting in Section 3.1, combined with 2MASS magnitudes to determine the individual magnitudes of the components. Since the system is not detected in the 2MASS $K_s$ band, we derived a 2MASS $K_s$ magnitude by computing a synthetic $J-K_s$ color of $0.45 \pm 0.07$ mag from the SpeX spectrum (e.g., Radigan et al. 2012), which implies a $K_s = 16.20 \pm 0.20$. The quoted uncertainty takes into account the relative component fluxes derived in Section 3.1, the photometric error reported in the 2MASS catalog, and uncertainties in our synthetic SpeX photometry, adding contributions from various sources in quadrature. Individual magnitudes and colors of the components are given in Table 5.

Since we have determined relative component fluxes and magnitudes more precisely than system magnitudes reported in 2MASS, we include values and uncertainties for the differential magnitudes between components, $\Delta J$, $\Delta H$, and $\Delta K_s$ in Table 5.

3.3.2. Spectral Types

We determined spectral types for the A, B, and C components using the resolved NIRC2 photometry and spectral templates of other field BDs from the SpeX Prism Library (e.g., Radigan et al. 2011) to decompose our unresolved system spectrum, and then decomposed the remaining BC contribution into individual B and C components. To perform the decomposition, we first identified all templates with spectral types $>0$ in the SpeX prism library sharing the same spectral resolution ($R \sim 120$) as our 2M0838+15 ABC spectrum. Since the relative color between components is much better constrained than the system color we first identified all templates sharing the same $J-K_s$ color as component A within 1σ uncertainties. For each A template we then identified templates for component BC falling within the observed $\Delta(J-K_s) \pm \sigma_{\Delta(J-K_s)}$ and $\Delta(J-H) \pm \sigma_{\Delta(J-H)}$.

Table 4

| Parameter | Value | Reference |
|-----------|-------|-----------|
| Identifier | J08381155+1511155 | 2 |
| $\alpha$ (J2000) | $08^h38^m11^s55^{.5}$ | 2 |
| $\delta$ (J2000) | $+15^\circ 11' 5^"$ | 2 |
| $\mu_\alpha \cos \delta$ ($''$) | $-0.121 \pm 0.031$ | 3 |
| $\mu_\delta$ ($''$) | $-0.032 \pm 0.051$ | 3 |
| $J$ | $16.65 \pm 0.16$ | 2 |
| $H$ | $16.21 \pm 0.17$ | 2 |
| $K_s$ | $16.20 \pm 0.20$ | 2 |
| $K_s^{A}$ | $0.45 \pm 0.07$ | 1 |
| $K_s^{B}$ | $0.51 \pm 0.07$ | 1 |
| $W1$ | $15.71 \pm 0.07$ | 3 |
| $W2$ | $14.57 \pm 0.3$ | 3 |

NIR SpT$^b$ $T3.5$ 1
$d$ (pc)$^c$ $49 \pm 12$ 1
$\rho_{BC}$ (mas) $50.2 \pm 0.5$ 1
$\theta_{BC}$ (deg) $-6 \pm 2$ 1
$\rho_{abc}$ (mas) $549 \pm 1$ 1
$\theta_{abc}$ (deg) $18.8 \pm 0.1$ 1
$\rho_{ABC}$ $0.89 \pm 0.92$ 1
$\psi_{BCA}$ $0.56 \pm 0.97$ 1

Notes.

$^a$ Synthetic 2MASS photometry from SpeX spectrum.

$^b$ Unresolved spectral type.

$^c$ Spectroscopic parallax.

$^d$ Range or value provided span values inferred for 0.3–3 Gyr.

References. (1) This work; (2) 2MASS Point Source Catalog (Skrutskie et al. 2006); (3) Aberasturi et al. (2011).

Table 5

| Parameter | A | B | C |
|-----------|---|---|---|
| NIR SpT | $T3 \pm 1$ | $T3 \pm 1$ | $T4.5 \pm 1$ |
| $J$ | $17.57 \pm 0.16$ | $18.04 \pm 0.16$ | $17.98 \pm 0.16$ |
| $H$ | $17.10 \pm 0.17$ | $17.43 \pm 0.18$ | $17.78 \pm 0.18$ |
| $K_s$ | $17.11 \pm 0.28$ | $17.46 \pm 0.20$ | $17.67 \pm 0.20$ |
| $\delta_{\text{MKO}}$ | $17.34 \pm 0.16$ | $17.81 \pm 0.16$ | $17.72 \pm 0.16$ |
| $\Delta_{\text{MKO}}$ | $0.52 \pm 0.04$ | $0.38 \pm 0.04$ | $0.38 \pm 0.04$ |
| $\Delta_{\text{MKO}}^{A}$ | $0.33 \pm 0.03$ | $0.47 \pm 0.05$ | $0.47 \pm 0.05$ |
| $\Delta_{\text{MKO}}^{B}$ | $0.35 \pm 0.02$ | $0.56 \pm 0.04$ | $0.56 \pm 0.04$ |
| $M$ (3 Gyr, $M_\odot$) | $0.060 \pm 0.009$ | $0.055 \pm 0.008$ | $0.050 \pm 0.008$ |
| $M$ (300 Myr, $M_\odot$)$^b$ | $0.020 \pm 0.005$ | $0.018 \pm 0.005$ | $0.016 \pm 0.004$ |

Notes.

$^a$ Differential magnitude with respect to component A.

$^b$ Masses at 300 Myr are multi-valued (see Figure 7). The high-mass solution for the 300 Myr isochrone is provided here.

3.2. Common Proper Motion

On 2010 March 22 follow-up images of the 2M0838+15 system were obtained in the $H$ and $CH_4$S (off-methane) filters using the NIRC2 narrow camera. Observing conditions were partially cloudy, the image FWHM was large ($\pm 0\farcs12$), and the BC components were not resolved. From fitting Gaussian PSFs to these data, relative positions and fluxes were determined between the A(BC) components. We found the ($CH_4S-H$) color of components A and BC to be indistinguishable within $\pm 0.05$ mag (with uncertainties inferred from 6 and 5 dithered images in the $CH_4$S and $H$ bands respectively), implying that the A and BC components have identical spectral types within $\pm 1$ subtypes according to the spectral type versus ($CH_4S-H$) relationship provided by Liu et al. (2008). This provided strong initial confirmation that the A(BC) components were both early–mid-T dwarfs. The 73 day separation between the first and second epoch NIRC2 images allowed us to confirm the common proper motion of the A(BC) components. Based on 2MASS, SDSS, and WISE epochs Aberasturi et al. (2011) determined a proper motion of $\mu = 0.13 \pm 0.06$ mas yr$^{-1}$ for the unresolved 2M0838+15 system (see Table 4), which would amount to a linear motion of $25 \pm 12$ mas between observations. We find the separation of the A(BC) components remains unchanged between 2010 January 8 ($548.6 \pm 1.2$ mas) and 2010 March 22 ($549.0 \pm 1.6$ mas) within a combined 2 mas uncertainty. This allows us to constrain the relative motions of the A(BC) components to within $\pm 10$ mas yr$^{-1}$, or a tenth of the system common proper motion. Given their similar spectral types, proximity on the sky, and shared proper motions within 10 mas yr$^{-1}$, we conclude that the 2M0838+15 ABC components are physically associated.
between A and BC components. The prospective A and BC templates were scaled to match the observed $H$-band fluxes of their respective components and added together to create a composite template. The composite templates were then interpolated onto the data and scaled in order to minimize $\chi^2 = \sum_i [\text{data}_i - \text{template}_i]^2 / \text{error}_i^2$. We scaled the error contribution in order to achieve $\chi^2 / \text{dof} = 1$ for the best-fitting model. Results are shown in Figure 6. Acceptable visual matches for the A(BC) components (deemed to occur for $\chi^2 / \text{dof} < 1.5$) range from T3–T4 with the optimal match for component A being the T3 dwarf SDSS J120602.51+281328.7 (Chiu et al. 2006), and the optimal match for component BC being the T3.5 dwarf SDSSp J175032.96+175903.9 (Geballe et al. 2002; Burgasser et al. 2006). We therefore estimate spectral types of T3 ± 1 and T3.5 ± 1 to the A and BC components, respectively.

The BC components were decomposed in a similar manner after subtracting the best fit for component A from the unresolved system spectrum. We found best-fitting templates with T3 (2MASS J12095613–100408; Burgasser et al. 2006) and T4.5 (SDSS J000013.54+255418.6; Burgasser et al. 2006) spectral types for the B and C components, respectively, with reasonable visual matches encompassing T2–T4.5 and T3–T5 spectral types. We therefore estimate spectral types of T3 ± 1 and T4.5 ± 1 for the unresolved B and C components. The results of our spectral decomposition are shown in Figure 6, and provide a reasonable match to the resolved OSIRIS A and BC spectra.

The similar spectral types found for the A and BC components are consistent with (CH$_4$ − $H$) colors found in Section 4, which indicate identical spectral types within ±1. In addition, the estimated A and BC spectral types agree well with the combined light spectral type of T3.5. Due to the low S/N of the OSIRIS spectra, as well as sub-ideal sky subtraction and telluric correction, we have not attempted to obtain spectral types by direct fits to these spectra, or from narrowband indices. In the future, higher S/N spectroscopy, possibly resolving all three components, should be attempted.

### 3.3.3. Absolute Magnitudes and Distance

Using the 2MASS $M_K$ versus SpT relation of Dupuy & Liu (2012) and magnitudes and SpTs derived above for the ABC components, we calculated an absolute magnitude and distance modulus for the individual A, B, and C components. We determined a mean distance modulus of 3.5 ± 0.5 mag, which implies a distance of 49 ± 12 pc. Distances inferred for the individual A, B, and C components of 46, 54, and 47 pc agree within uncertainties, yet reflect the similar spectral types despite different brightnesses for the A and B components. Given
uncertainties take into account uncertainties in the measured magnitudes and spectral types of the components, as well as intrinsic scatter of \(\sim 0.46\) mag about the Dupuy & Liu et al. relationship.

At a distance of 49 pc and assuming the semimajor axes to be similar in length to their projections (a reasonable assumption given correction factors of \(a/\rho = 0.85\)–1.16 for visual VLM binaries in Dupuy & Liu 2011), the system would have physical separations of \(2.5 \pm 0.5\) AU (BC) and \(27 \pm 5\) AU (A[BC]) respectively.

3.3.4. Relative Masses, Effective Temperatures, and Surface Gravities

Without an independent measurement of mass or age, evolutionary models are degenerate and prevent absolute physical properties from being inferred. However, assuming the components of the ABC system to be coeval we can infer relative properties for a reasonable range of ages. We estimated bolometric luminosities using the updated MKO-\(K\)-band bolometric corrections provided by Liu et al. (2010), first converting 2MASS \(K_s\) magnitudes to MKO magnitudes using the corrections as a function of spectral type provided by Stephens & Leggett (2004). The differences in bolometric corrections between components is small, with a maximum difference of \(0.013\) mag (2004). The differences in bolometric corrections between components is small, with a maximum difference of \(0.013\) mag (2004). The differences in bolometric corrections between components is small, with a maximum difference of \(0.013\) mag.

For a given system age these luminosity estimates can be converted to masses, effective temperatures, radii, and surface gravities via evolutionary models. We used the evolutionary models of Burrows et al. (1997) to infer masses, effective temperatures, and surface gravities at ages of 3 Gyr (typical for field BDs) and 300 Myr. For a 3 Gyr old system we find masses of 60, 55, and \(50 \times 10^{-3}\) \(M_\odot\) with a systematic uncertainty of \(\sim 15\%\) and relative uncertainties of \(\sim 3\%\). For an age of 300 Myr we find masses of 20, 18, and \(16 \times 10^{-3}\) \(M_\odot\) with a systematic uncertainty of \(\sim 25\%\) and relative uncertainties of \(\sim 5\%\) (we note that there are degenerate solutions for this age, which yield component masses as low as \(\sim 0.13\)–\(0.14\) \(M_\odot\); see Figure 7). The largest source of uncertainty factoring into these calculations comes from the absolute magnitude determination.

In both cases the mass ratio of the BC components \(q_{\text{BC}}\) is close to unity (0.92 for 3 Gyr and 0.89 for 300 Myr), which is typical for BD binaries which are found to have a mass ratio distribution peaking strongly at unity (e.g., Burgasser et al. 2007; Allen 2007; Liu et al. 2010). While the A(BC) mass ratio of \(\sim 0.57\) would be atypically low compared to the majority of BD binaries, near-equal mass A, B, and C components for VLM triple systems are common (e.g., Burgasser et al. 2012).

In order to estimate a range in surface gravities and temperatures spanned by the ABC components we have plotted inferred effective temperatures and surface gravities along a series of isochrones ranging from 300 Myr to 5 Gyr, shown in Figure 7. For ages of 0.5–5 Gyr \(d(\log g)/d(T_{\text{eff}})\) is approximately constant along isochrones, with the ABC components spanning a fairly narrow range in temperature (\(\sim 150\) K) and surface gravity (\(\sim 0.1\) dex) irrespective of age or mass.

Given the inferred system masses and a semimajor axis of 2.5 AU, the BC system would have a period ranging from \(\sim 12\) yr (3 Gyr) to \(\sim 21\) yr (300 Myr). Thus a dynamical mass measurement of the BC components may be possible on a relatively short timescale, which should greatly constrain the system’s position in Figure 7. In addition, efforts to obtain a parallax are ongoing, which will provide improved constraints on the system’s absolute magnitude and bolometric luminosity.

4. SEARCH FOR COMPANIONS AND SENSITIVITY LIMITS

Here we present our search for companions around the entire sample of eight L/T transition objects observed with NIRC2 (Section 2.2).

Each reduced image was carefully visually examined for companions. Only a single object, 2M0838+15, was resolved into a multiple system. Our sensitivity to companions was determined via simulations. For a given binary separation, \(\rho\), and contrast, \(\Delta K\), we constructed 100 simulated binary pairs using a cutout of the observed target as a single PSF model, with randomized position angles. We then attempted to recover companions from the simulated images in the following way:

1. We first subtracted off a 51 pixel median filter of the input image in order to remove any sloping background and then iteratively measured the rms background noise (i.e., in regions without a source) of the simulated image, \(\sigma\).
2. We searched for point sources in the image using the IDL adapted version of the DAOPHOT find algorithm, setting a 5\(\sigma\) detection threshold.
3. For each of the candidates identified by find we measured the rms noise in a 1 FWHM wide annulus with a mid-radius...
corresponding to the distance to the candidate source. The candidate source itself was masked using a circular region with 0.75 FWHM radius. Candidates at separations greater than 350 mas and with peak fluxes less than five times the noise within the annulus were discarded. For candidates at separations less than 350 mas we enforced a slightly higher detection threshold of seven times the noise, due to the presence of high frequency structure in the AO PSF in this region.

4. A further search for close (blended) companions inside 200 mas was conducted. Low frequency features were subtracted from the simulated image using a median-filtered image (wherein each pixel is replaced by the median of surrounding pixels in a box size of 1 × 1 FWHM rounded up to the nearest odd-integer number of pixels). We then repeated our search for additional peaks using find. Sources with peak fluxes <0.15 times that of the central source were discarded. This detection limit corresponds to roughly three times the size of the largest residuals found when subtracting a Gaussian PSF from our data.

The above criteria were verified by visual inspection and consistently picked out bona fide companions in our simulated datasets, while rejecting other point-source-like structures in the AO PSFs. We note that since the PSF is significantly different for each target (dependent on the relative position and brightness of the TT star used) we were unable to build a model of a single PSF to subtract from those of our targets. When applied to the data, the above criteria successfully detect the close 2M0838+15BC pair in the science images wherein ρBC > 0.5 FWHM, while assigning non-detections to the other sources in our sample. Our sensitivity to companions at a given separation is given by the recovery rate of simulated companions, and is shown for each source in Figure 8.

Although varying from target to target, we are sensitive to approximately 95% of companions with ΔK < 1 at innermost separations of 60–120 mas, and to companions with contrasts of ΔK > 2.5–4 at separations > 200 mas. The tight BC components of 2M0838+15 fall inside the minimum separation where companions are routinely detectable. We easily resolve the BC pair due to the fact that the binary axis runs approximately perpendicular to the PSF elongation in the direction of the TT star. In other words, sensitivity is a function of position angle for elongated PSFs, and the 95% recovery rates reported reflect the least sensitive position angles.

4.1. The Binary Fraction of our Sample

In our sample we resolved 1 of 8 targets into a multiple system (we do not count 2M0838+15 BC as an additional target). The probability of observing n multiples in our sample is given by the binomial distribution, P(n|N = 8, νobs), where νobs is the observed binary frequency (uncorrected for observational biases), n is the number of binaries observed, and N is the sample size. A Beta distribution for νobs is obtained by using Bayes’ Law.

**Figure 8.** K-band detection limits as a function of binary separation and contrast, ΔK. Red lines indicate the 95% recovery rate of simulated companions. The shading depicts the recovery rate for any separation and contrast, linearly varying from 0% (black) to 100% (white).

(A color version of this figure is available in the online journal.)
Table 6
The Composite L9–T4 Sample

| 2MASS ID          | SpT  | J    | J − Ks | m − M | d (pc) | θ (″) | Reference
|-------------------|------|------|--------|-------|--------|-------|-----------|
| 2MASS J01191207+2403317 | T2   | 17.02 ± 0.18 | 1.00 ± 0.26 | 2.51 ± 0.50 | 31.8 ± 6.6  | 3.36 | 4         |
| 2MASS J01365662+0934373 | T2.5 | 13.45 ± 0.03 | 0.89 ± 0.04 | −1.07 ± 0.46 | 6.1 ± 1.3  | 3     |
| 2MASS J01514155+1244300 | T1   | 16.57 ± 0.13 | 1.58 ± 0.23 | 1.92 ± 0.50 | 21.4 ± 1.5 | 2     |
| 2MASS J02474978−1631132 | T2   | 17.19 ± 0.18 | 1.57 ± 0.27 | 2.11 ± 0.50 | 26.5 ± 5.5  | 4     |
| 2MASS J03264265+2302051 | L9.5 | 16.69 ± 0.14 | 1.78 ± 0.18 | 1.97 ± 0.47 | 30.2 ± 3.8  | 10, 1, 5 |
| 2MASS J03510423+4810477 | T1   | 16.47 ± 0.13 | 1.47 ± 0.18 | 1.73 ± 0.48 | 22.2 ± 4.6  | 4     |
| 2MASS J04234858+0933473 | T2   | 14.95 ± 0.04 | 1.07 ± 0.07 | 0.38 ± 0.46 | 11.9 ± 2.5  | 4     |
| 2MASS J03871718−0000179 | T1   | 17.10 ± 0.21 | 1.23 ± 0.30 | 2.61 ± 0.51 | 30 ± 12     | 2     |
| 2MASS J09083803+5032088 | L9   | 14.55 ± 0.02 | 1.60 ± 0.04 | 0.10 ± 0.46 | 10.5 ± 2.2  | 5     |
| 2MASS J09201223+3517429 | T0p  | 15.62 ± 0.06 | 1.65 ± 0.09 | 0.93 ± 0.46 | 29.1 ± 0.7  | 0.057  |
| 2MASS J10210969−0304197 | T3   | 16.25 ± 0.09 | 1.13 ± 0.20 | 1.35 ± 0.49 | 33.4 ± 1.5  | 0.172  |
| 2MASS J12545393−0122474 | T2   | 14.89 ± 0.04 | 1.05 ± 0.06 | 0.33 ± 0.46 | 11.8 ± 0.3  | 3     |
| 2MASS J14044941−3159329 | T2.5 | 15.58 ± 0.06 | 1.04 ± 0.11 | 0.90 ± 0.47 | 23.8 ± 0.6  | 3     |
| 2MASS J17503293+1759042 | T3.5 | 16.34 ± 0.10 | 0.86 ± 0.21 | 1.54 ± 0.50 | 27.6 ± 3.5  | 2     |
| 2MASS J20474959−0718176 | T0   | 16.95 ± 0.20 | 1.57 ± 0.28 | 2.33 ± 0.50 | 20.0 ± 3.2  | 3     |
| 2MASS J22541892+3123498 | T4   | 15.26 ± 0.05 | 0.36 ± 0.15 | 0.80 ± 0.48 | 14.4 ± 3.0  | 2     |

Notes.

- a Unresolved NIR spectral type.
- b Survey references.
- c Parallax references. Distances without parallaxes are based on the SpT versus absolute K, magnitude relationship of Dupuy & Liu (2012).

References. (1) Bouy et al. 2003; (2) Burgasser et al. 2006; (3) Goldman et al. 2008; (4) This paper; (5) Reid et al. 2006; (6) Dahn et al. 2002; (7) Vrba et al. 2004; (8) Dupuy & Liu 2012; (9) Faherty et al. 2012; (10) Gizis et al. 2003; (11) Reid et al. 2001.

5. BINARY STATISTICS IN THE L/T TRANSITION

5.1. The L9–T4 Binary Frequency

The L/T transition is roughly the regime over which condensate clouds disappear as a major opacity source in BD photospheres. Here we consider the L/T transition to encompass L8–T5 spectral types, which is the range associated with J-band brightening. We have chosen not to include the ends of this branch (L8 and T5 bins) in our analysis so as not to contaminate the sample with objects of ambiguous membership. There is a long standing question as to whether the binary fraction might be larger inside the transition. Burgasser (2007) demonstrated with simulations that a flattening of the luminosity function for single objects within the L/T transition will result in a sparsity of objects in these spectral type bins. Combined with no such flattening of the unresolved binary luminosity function at similar spectral types, this results in an enhanced binary fraction. However, evolutionary models used by Burgasser (2007) did not account for cloud evolution, and more recent evolutionary models including evolving clouds (Saumon & Marley 2008) predict a pileup rather than deficit of objects at the cloudy/clear transition. Thus, observations of the L/T transition binary fraction can provide a useful test for evolutionary models. Additionally, the L/T transition is the spectral type range over which variability may be expected due to heterogeneous cloud coverage (e.g., Burgasser et al. 2002; Radigan et al. 2012), and the level of binary contamination in this regime has important consequences for variability surveys (e.g., Clarke et al. 2008; Radigan et al. 2011).

Although small, our sample increases the number of objects observed with L9–T4 spectral types by 40%. If taken together with the L/T transition sample observed by Goldman et al. (2008), these more recent data nearly double the number of objects surveyed for multiplicity in this regime. Here we combine our data with the L/T transition survey of Goldman et al. (2008), T-dwarf surveys of Burgasser et al. (2003, 2006), and the combined L and T samples of Bouy et al. (2003) and Reid et al. (2006, 2008) to examine the binary frequency in the L/T transition.

5.1.1. The Combined Statistical Sample

Although the surveys considered are a heterogeneous group, they are all sensitive to minimum angular separations of approximately 0.05–0.1′′. In addition, ultra cool dwarf binaries tend to have flux ratios well above typical detection limits (except at small angular separations), implying that differing sensitivities to faint companions among surveys does not strongly impact binary statistics (e.g., Burgasser et al. 2007; Allen 2007). To achieve consistency each target was cross-correlated with the DwarfArchives database of known L and T dwarfs to determine a homogeneous set of NIR spectral types and colors. Names, spectral types, and J − Ks colors of the combined sample are provided in Table 6.

In total the combined sample consists of 19 objects including 2M0838+15 with NIR spectral types of L9–T4 (inclusive).
However, as the only known higher order multiple in the sample, 2M0838+15 is significantly farther away \((d \sim 50 \text{ pc})\) than other objects of the sample \((d < 35 \text{ pc})\) and likely biases the result. Rather than attempting a completeness correction for higher order multiples we apply a 35 pc distance cut, which effectively removes 2M0838+15 from the targets considered, yielding a final sample size of 18.

Based on 4/18 detections in the L9–T4 sample, we computed \(P(v_{\text{obs}}|n, N) \propto P(n|N, v_{\text{obs}})\) as in Section 4.1, obtaining an observed binary fraction for the combined sample of \(v_{\text{obs}} = 22^{+10\%}_{-8\%}\). This is on the high end, but comparable to other reported visual binary fractions for L and T dwarfs (subject to similar selection effects and observational constraints, and uncorrected for biases) previously discussed in Section 4.1 (\(\sim 17\%–20\%\)).

### 5.1.2. Correcting for Observational Biases

In magnitude limited samples a Malmquist bias leads to binaries being sampled in a larger volume than singles. Here we follow the example of Burgasser et al. (2003, 2006) who provide an expression for the real binary frequency, \(v\), in terms of the observed frequency, \(v_{\text{obs}}\):

\[
v = \frac{v_{\text{obs}}}{\alpha(1 - v_{\text{obs}}) + v_{\text{obs}}},
\]

where \(\alpha\) is the ratio of volume searched for binaries to that of the volume searched for single objects given by

\[
\alpha = \frac{\int_0^1 (1 + \rho)^{3/2} f(\rho) d\rho}{\int_0^1 f(\rho) d\rho},
\]

where \(\rho = f_2/f_1\) is the flux ratio of components and \(f(\rho)\) is the distribution of flux ratios. The limiting cases where \(f(\rho)\) is flat and 100% peaked at unity yield values of \(\alpha = 1.86\) and \(\alpha = 2.82\), respectively, and typically an intermediate value is used. However, if we examine the distribution of flux ratios for all known L and T binaries (see the Appendix) we find a broad distribution that peaks at \(\sim 0.4–0.5\) with a negative skew, such that the mean flux ratio is slightly larger than this. Integrating over this distribution we obtain \(\alpha = 1.87\), which is equivalent to the case where \(f(\rho)\) is flat. As a check, the binaries in our sample have flux ratios (in their survey filter, see Table 6) ranging from 0.39–0.46 which yield an average value of \((1 + \rho)^{3/2} = (d_{\text{bin}}/d_{\text{single}})^3\) of 1.7. As a compromise between the two values, we adopt a value of \(\alpha = 1.8\) for our sample.

To correct for our greater sensitivity to binaries over single objects, we performed a change in variables from \(v_{\text{obs}} \rightarrow v\):

\[
P(v) = P(v_{\text{obs}}) \frac{dv_{\text{obs}}}{dv},
\]

where a relationship between \(v\) and \(v_{\text{obs}}\) is given in Equation (3).

From the resulting distribution we calculated the most probable binary frequency and uncertainties corresponding to a 68% shortest credible interval, shown in Figure 9. This yielded a resolved L9–T4 binary fraction of \(13^{+7}_{-5}\%\) at projected separations \(\geq 1–2.5\ \text{AU}\). It is important to note that this is only the visual binary frequency for the stated detection limits and ignores the small-separation wing of the semimajor axis distribution. By some estimates spectroscopic binaries could be as numerous as resolved systems (Maxted & Jeffries 2005; Joergens 2008), increasing the total binary fraction by a factor of two.

For comparison, the T-dwarf surveys of Burgasser et al. (2003) and Burgasser et al. (2006) found bias-corrected binary fractions of \(8^{+5}_{-3}\%\) and \(12^{+7}_{-4}\%\) (but used a slightly larger value of \(\alpha = 2.16\)), while the late-M and L-dwarf surveys of Bouy et al. (2003) and Reid et al. (2008) found binary fractions of \(\sim 10\%\) and \(12^{+5}_{-4}\%\), respectively (the latter survey was volume-limited). While we find a slightly higher binary frequency from L9–T4 spectral types, it remains comparable to those reported by other surveys at the 1\sigma level.

It is nonetheless interesting to note that if we select the L9–T4 sample based on primary spectral types rather than unresolved system types the observed binary fraction drops to \(2/16 (=12.5\%)\), which translates into a bias-corrected frequency of \(6^{+6}_{-4}\%\) or about half of the unresolved fraction (resolved spectral types of binaries for the surveys considered here are provided in Table 7). Thus even though we do not find a statistically significant increase in binary fraction for L9–T4 spectral types relative to other L- and T-dwarf samples, there is some evidence of a systematic increase in binary frequency between unresolved and primary spectral-type-selected samples by a factor of \(\sim 2\). This is consistent with the population synthesis of Burgasser (2007), which shows that the binary frequency approximately doubles for unresolved L9–T4 dwarfs given a flat input distribution as a function of primary spectral type. In addition, we cannot rule out an L9–T4 binary frequency as high as \(21\%\) (the upper limit of our 68% credible interval), and it therefore remains possible that the unresolved binary frequency is much higher in the L/T transition. Clearly, a larger sample of L/T transition objects is needed to make progress.

### 6. DISCUSSION AND CONCLUSIONS

#### 6.1. 2M0838+15ABC: A Benchmark Triple of Early-T Dwarfs

We have presented resolved imaging and spectroscopy of the first triple T-dwarf system, 2M0838+15 ABC.

With a dynamical mass measurement possible for the BC components, 2M0838+15 ABC will serve as a benchmark system in the poorly contained L/T transition regime. Even without a dynamical mass, this system represents the largest...
homogeneous sample of early-T dwarfs to date, whose relative colors and spectral types can be used to test evolutionary models along a single isochrone.

The relative positions of the A, B, and C components on a color–magnitude diagram are shown in Figure 10. We find that component A, which is brightest in all three bandpasses, has a J − Ks color intermediate to the fainter B and C components.

Alternatively, different condensate cloud properties could explain differences in brightness between components A and B without the need to invoke differences in surface gravity. Observations of variable BDs have demonstrated that changes in cloud coverage at constant effective temperature, surface gravity, and empirical spectral type can lead to brightness variations as high as ∼0.1 dex for ages greater than 300 Myr.

Assuming for now that 2M0838+15 does not vary in brightness, we explore the possibility that systematic differences in cloud properties between the A and BC components could be due to viewing geometry. For instance, if the tight BC components have spin axes that are aligned with each other but not with the wider component A, the difference in relative cloud properties may reflect pole-on versus edge-on orientations of banded clouds. There is some evidence both observationally (Hale 1994; Monin et al. 2006) and in hydrodynamic radiative simulations of star formation (Bate 2012) that close binary components likely to have a severely misaligned component from three-body dynamics. However, recent observations by Konopacky et al. (2012) of 11 VLM binaries cast some doubt on this hypothesis. These authors find nearly half of their sample (5/11) of highly different v sin i (all with separations <5 AU) which may indicate frequent spin misalignment in close VLM binaries (although this could also reflect intrinsically different rotation rates).
6.2. Formation and Dynamical Stability of 2M0838+15

The 2M0838+15 ABC system stands out as the only known T-dwarf triple system to date, and furthermore the only known BD triple system where all three components have been directly and conclusively detected. There are only two other examples of possible or probable BD triple systems in the literature: Kelu-1 (Ruiz et al. 1997; Liu & Leggett 2005; Stumpf et al. 2008) and DENIS-P J020529.0−115925 (Delfosse et al. 1997; Koerner et al. 1999; Bouy et al. 2005), although in former cases the tertiary component remains unresolved and in both cases flux ratios and separations cannot be accurately determined. There are a handful of VLM triples (seven known or suspected to date) discussed in Burgasser et al. (2012), and of these only two prove to be good analogs to 2M0838+15 ABC with near-equal component masses and relatively low ratios of outer-to-inner separations: (1) LP 714-37, an M5.5/(M8/M8.5) triple with similar component masses of 0.11, 0.09, and 0.08 $M_\odot$, and outer/inner separations of 33 AU/7 AU; (2) LHS 1070 ABC, a (M5/M8.5/M9) triple with component masses of 0.12, 0.08, and 0.08 $M_\odot$ and separations of 12 AU and 3.6 AU (Leinert et al. 2001; Seifahrt et al. 2008). The other known VLM triples have much larger inner-to OUTER SEPARATION RATIOS ($\geq$100), which implies a multimodal distribution of inner-to-outer period ratios as is seen for higher mass triples (e.g., Tokovinin 2008).

Hydrodynamic simulations of fragmentation and subsequent evolution in a gas-rich environment (e.g., Bate et al. 2002b; Bate 2009, 2012) can form triples at separations smaller than the fragmentation scale ($\leq$100–1000 AU) and with preference for equal masses as a result of dissipative interactions with disks, and accretion. These simulations successfully produce VLM and BD triples with outer-to-inner separation ratios of $\sim$10–100. The role, if any, of subsequent dynamical interactions within a gas-free cluster is unclear. Simulations of gravitational interactions between small-$N$ cluster members by Sterzik & Durisen (2003) and Delgado-Donate et al. (2004) can infrequently produce BD triples ($\sim$0.2% of all triple systems), but this mechanism does not reproduce observed properties of binaries (it leaves larger populations of single stars and close binaries than are observed; Goodwin & Kroupa 2005), or higher mass triples (observed triples have broader period distributions, larger outer-to-inner period ratios, and mass ratios closer to unity than those formed in simulations; Tokovinin 2008), and therefore is unlikely a major determinant of stellar multiplicity properties in general.

Nonetheless, there is nothing that rules out this scenario for the 2M0838+15 ABC system in particular, and the outer-to-inner period ratio of $\sim$10 is similar to those produced from dynamical decay simulations. Furthermore, there is debate as to whether dynamical ejection (e.g., Reipurth & Clarke 2001; Bate et al. 2002a) of BD systems from the surrounding gas reservoir, while accretion is still ongoing, may be required to halt further growth and prevent proto-BDs from reaching stellar masses.

For an age of 3 Gyr we find an approximate binding energy of $\sim$20 $\times$ 10$^{41}$ erg, satisfying the minimum binding energy typically found for VLM binaries (e.g., Close et al. 2003; Burgasser et al. 2007). If this binding energy cutoff is the result of dynamical ejection then the 2M0838+15 ABC system is likely to have survived such an event. Alternatively, for an age of 300 Myr the system would have a binding energy of $\sim$1.6 $\times$ 10$^{41}$ erg, well below the empirical minimum, and join only a handful of similarly weakly bound VLM and BD systems (see Figure 11). This observation may favor an older age for 2M0838+15 ABC.

With an inner-to-outer ratio of projected separations of $\sim$10, the 2M0838+15 ABC system currently satisfies the stability criterion suggested by Eggleton & Kiseleva (1995) of $Y_0 > 6.7$, where $Y_0$ denotes the ratio of inner binary apastron separation, versus the outer binary periastron separation. Due to projection effects the actual inner-to-outer separation ratios could be even larger than measured. Assuming that the outer-to-inner ratio of semimajor axes is close to the observed ratio of projected separations ($\sim$10) implies a period ratio of $\sim$30 for the inner
and outer orbits. In this case the empirical stability criterion for
Figure 11. Binding energy as a function of total mass for stellar and VLM
binary systems. The 2M0838+15 A(BC) system is plotted using a five-point
star. A dotted horizontal line makes the minimum binding energy cutoff of
∼20 × 10^{31} \text{erg} observed for the majority of VLM binaries. Most of the other
VLM binaries plotted (squares) are taken from the VLM Binary Archive, which
is a compilation of data from 144 unique publications which can be accessed
at vlmbinaries.org. Additional VLM systems, stellar binaries (crosses), and
stellar primaries with VLM secondaries (open circles) are taken from Close
et al. (1990), Fischer & Marcy (1992), Tokovinin (1997), Reid & Gizis (1997a,
1997b), Reid et al. (2001), Caballer et al. (2006), Daemgen et al. (2007),
Kraus & Hillenbrand (2007), Radigan et al. (2008), Luhman et al. (2009), and
Faherty et al. (2010). Young/low-gravity systems are marked by filled circles
and squares.

and outer orbits. In this case the empirical stability criterion of
Tokovinin (2004), \( P_{\text{out}}(1 - e_{\text{out}}^2)/P_{\text{in}} > 5 \), is satisfied for outer eccentricities of \( e_{\text{out}} \lesssim 0.45 \). Thus current observations are
consistent with the long-term stability of the 2M0832+15ABC system.

6.3. Binarity at the L/T Transition

We have found a late-L/T transition binary frequency (L9–T4
spectral types, at observed separations \( >0.05-0.1 \) ) of \( 13^{+7}_{-6}\% \). This is similar to reported frequencies outside of the transition
(Burgasser et al. 2003, 2006; Reid et al. 2008; Bouy et al. 2003,
\( \sim9\%-12\% \)). This preliminary result provides an optimistic
outlook for studies of L/T transition BDs: it suggests that this
sample is not significantly contaminated (or at least not much
more so than other ultracool dwarf populations) by binaries
whose combined spectra mimic those of bona fide L9–T4
dwarfs. On the other hand, we found the unresolved L9–T4
binary fraction to be double that of a primary-spectral-type-
dwarfs. On the other hand, we found the unresolved L9–T4
whose combined spectra mimic those of bona fide L9–T4
unsolved spectral types. In this case, the actual unresolved L9–T4 binary frequency could be on the high end of our inferred distribution for \( v \) (e.g., \( \sim20\% \) at the 1σ upper limit). A larger sample will be required to resolve
these contradictory indications.

Burgasser et al. (2010) asked the question of whether L/T
transition binaries may be identified from their NIR spectra.
This would be advantageous as it would allow us to improve
our statistical studies and to identify binary contaminants in the
L/T transition regime. The authors compared the NIR spectra
of L/T transition dwarfs to a series of single and composite
spectral templates and identified objects with spectral features
common to known binaries as “strong” and “weak” binary can-
didates depending on the number of common traits. Our sam-
ple contained two “strong” binary candidates (2M0247+16 and
2M0351+48) and two “weak” binary candidates (2M0119+24
and 2M0758+32) suggested by Burgasser et al. (2010), and
none were resolved into multiples. This result suggests that
either (1) we cannot identify binaries reliably using spectral ind-
ces, or (2) the estimated number of binaries missed at low
separations is significant. In all likelihood both of these expl-
ations are partially true. In the first case, spectral irreg-
ularities in the candidate binaries may be caused by atypical
atmospheric or physical properties, rather than binarity. This is
likely the case for another strong candidate binary of Burgasser
et al. (2010), 2M2139+02, which was found to have peculiar at-
mospheric characteristics (patchy clouds, and large-amplitude
photometric variability; Radigan et al. 2012). Alternatively,
the second explanation may find support in radial velocity surveys
of VLM stars and BDs both in the field or in young clusters
(e.g., Maxted & Jeffries 2005; Basri & Reiners 2006; Joergens
2008) which show that there may be just as many binaries at
separations <3 AU as found by direct imaging surveys. In this
latter case the true L9–T4 binary frequency could be as high as
\( \sim30\%-40\% \). Even so, this would imply that the majority
(\( \sim2/3 \) ) of objects in the late-L/T transition are single.

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APPENDIX

THE EMPIRICAL FLUX RATIO DISTRIBUTION OF
RESOLVED L- AND T-DWARF BINARIES

In order to convert the observed binary fraction into a volume-
corrected binary frequency using Equation (3) we needed to
compute the ratio of volume searched for binaries over single
objects, \( \alpha = (d_{\text{bin}}/d_{\text{single}})^3 \). To do this we used Equation (4)
which is originally given in Burgasser et al. (2003), and depends
on the distribution of flux ratios for resolved binaries, \( (f_2/f_1) \).
The contrasts, \( \Delta m \), for known binaries reported by Burgasser
et al. (2003, 2006), Bouy et al. (2003), and Reid et al. (2006,
2008) are given in Table 7. We converted these contrasts to
flux ratios according to $f_2/f_1 = 10^{-0.4 \Delta m}$. This empirical flux ratio distribution is shown in Figure 12. Integrating directly over this empirical distribution in Equation (3) we found $\alpha = 1.87$, which is almost identical to the value obtained for a flat flux ratio distribution of $\alpha = 1.86$.

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Figure 12. Distribution of flux ratios for resolved L- and T-dwarf binaries in Table 7 (black histogram). Colored bars show how the sample subdivides by unresolved spectral type. Integrating over this empirical distribution using Equation (4), we find $\alpha = 1.87$, which is equivalent to the value for a flat distribution, and strongly differs from the value found by assuming flux ratios peak at 1.

A color version of this figure is available in the online journal.

Yelda, S., Lu, J. R., Ghez, A. M., & et al. 2010, ApJ, 725, 331