Economic impact due to Cimanuk river flood disaster in Garut district using Cobb-Douglas analysis with least square method

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Abstract. Cimanuk River, Garut District, West Java which have upper course in Papandayan Mountain have an important purpose in daily living of Garut people as a water source. But in 2016 flash flood in this river was hit and there was 26 people dead and 23 people gone. Flash flood which hit last year make the settlement almost align with the ground, soaking school and hospital. BPLHD Jawa Barat saw this condition as a disaster which caused by destroyed upper course of Cimanuk River. Flash Flood which happened on the 2016 had ever made economic sector paralyzed. Least square method selected to analyze economic condition in residents affected post disaster, after the mathematical equations was determined by Cobb Douglas Method. By searching proportion value of the damage, and the result expected became a view to the stakeholder to know which sector that become a worse and be able to make a priority in development.

Keyword : Cobb Douglas, Least Square Method, Proportion value

1. Introduction
Since long time ago, people have settled near the river and today this condition still continued. River becomes one choice for transportation, provides a water for industry and agriculture also be able to increase the quality of life because living in the middle of a beautiful nature. But, living near a river have a risk of flood, one of the most dangerous disaster on earth [1]. Cimanuk River location in Garut Resident, West Java, Indonesia which the upstream in Papandayan Mountain have an important role in daily life of Garut citizen such as a source of water. In 2016, was happened a big flash flood in this river and as a consequence there was 26 deaths dan 23 gone also the the economic activity was paralyzed. BPLH (Environmental Management Agency) Jawa Barat saw this condition caused by the damaged land in upstream of Cimanuk River. The flash flood in Cimanuk River in 2016 was the most damage flood ever in Garut. Data from BPLHD (Disaster Management Agency) Garut Resident showed that economic lost in that disaster touch 671 billion rupiahs [2]. In this case, the civilization activity still
near river like hospital, school and housing that means just only upstream and river revitalization can make this disaster stopped. In the other side, upstream revitalization need a time so this this paper aimed to model the economic lost if the condition still the same.

Some research related to this paper are Develop a dynamic optimization model, where inter-temporal decision of an economic agent are interacts with the hydrological system [3]. Input-Output Tables used to study the analysis of the economic impact of a Natural Disaster Tokai Flood in 2000 in Japan [4]. They proposed analysis methodology to estimate returns to scale in case of Cobb-Douglas production function [5]. Partial least square used to identify the information about the correlation of multivariate cognitive abilities and local brain structure in children and adolescents [6].

This paper showed the mathematical model which formed by Cobb-Douglas Method and the index and constant gotten by Partial Least Square Method. The main data was generated by normal distribution. This paper aims to derive a mathematical model of Cimanuk river flash flood, that can be used to predict the total of economic lost

2. Preliminaries
This section describe the main theoretical tools that used to formed mathematical model for flash flood in Cimanuk River.

2.1. Cobb-Douglas Method.
Cobb-Douglas production function is a function or a model that involves a dependent variable and two or more independent variables. The model can be written as follow:

\[ Y = aX_1^bX_2^c \]  

Where:
- \( Y \) is an output
- \( a \) is an efficiency index
- \( X_1, X_2 \) is a kind of input
- \( b, c \) is a production elasticity from the used input

In order for data to be obtained can be analysed by Cobb-Douglas Method, so the data must be transformed into a linear form by using natural Logarithm (Ln). The model showed:

\[ \ln Y = \ln a + b \ln X_1 + c \ln X_2. \]  

and transform back to (1) [7]

2.2. Partial Least Square Method
Partial Least Square (PLS) Method designed to be an alternative from Structural Equation Modelling (SEM) which used to solved the condition between variable really complex but the sample size is small [8]. This method was introduced by Herman O.A Wold to forming a prediction model. (Talbot) PLS used to predict the effect of X variable to Y variable and explained the theoretical correlation between the variable. PLS is a regression method that can be used to identify the factor which combination X variable as an explanation and Y variable as a response.

PLS regression is a method to find a component from X variable which have correlation with Y variable. The concept of PLS regression is describing Y variable as a response and X variable as a predictor by equation:

\[ y = Tq^T + f \]  
\[ x = TP^T + E \]

Where :
- \( y \) is a vector variable response
- \( x \) is a predictor variable matrix
- \( T \) is a PLS component score
- \( q \) is a vector loading from y
P is a factor loading matrix from x 
Vector Q obtained from the regression the indicator variable with the PLS component score using Ordinary Least Square (OLS) [9]

2.3 Significance Test
2.3.1 Significance Test (F statistics test)
The F test aims to determine the significance of the correlation of independent variable to dependent variable. The F test is done by comparing the value of F-test and F-table with a level of significant 95%.

The way to test the hypothesis are:
1. Determine the hypothesis
   \[ H_0 = \text{the lost of housing, lost of infrastructure, lost of social criteria, lost of economic source and lost of cross sector simultaneous do not have a correlation into the economic impact.} \]
   \[ H_1 = \text{the lost of housing, lost of infrastructure, lost of social criteria, lost of economic source and lost of cross sector simultaneous have a correlation into the economic impact.} \]

2. Determine the level of significant (\( \alpha \))
   In this case, the level of significant is 5% with the level of confidence 95%

3. Determine the Testing Criteria
   \[ H_0 \text{ is not accepted if } F\text{-test} > F\text{-table} \]
   \[ H_1 \text{ is accepted if } F\text{-test} \leq F\text{-table} \]

4. Conclusion
   If \( H_0 \) not accepted so the lost of housing, lost of infrastructure, lost of social criteria, lost of economic source and lost of cross sector simultaneous have a correlation into the economic impact.
   If \( H_1 \) accepted so the lost of housing, lost of infrastructure, lost of social criteria, lost of economic source and lost of cross sector simultaneous have a correlation into the economic impact.

2.3.2 Wald Test (t test)
Test t aims to determine the differences of each other data by means. The t test also showing how significant the difference are. The t test is done by comparing the value of t-test and t-table with a level of significant 95%. The way to test the hypostasis are:
1. Determine the hypothesis
   a) \( H_{01}; \beta_1 = 0 \), lost of housing as a partial have no correlation to economic impact.
      \( H_{11}; \beta_1 \neq 0 \), lost of housing as a partial have correlation to economic impact.
   b) \( H_{02}; \beta_2 = 0 \), lost of infrastructure as a partial have no correlation to economic impact.
      \( H_{12}; \beta_2 \neq 0 \), lost of infrastructure as a partial have correlation to economic impact.
   c) \( H_{03}; \beta_3 = 0 \), lost of social criteria as a partial have no correlation to economic impact.
      \( H_{13}; \beta_3 \neq 0 \), lost of social criteria as a partial have correlation to economic impact.
   d) \( H_{04}; \beta_4 = 0 \), lost of economic as a partial have no correlation to economic impact.
      \( H_{14}; \beta_4 \neq 0 \), lost of economic as a partial have correlation to economic impact.
   e) \( H_{05}; \beta_5 = 0 \), lost of cross sector as a partial have no correlation to economic impact.
      \( H_{15}; \beta_5 \neq 0 \), lost of cross sector as a partial have correlation to economic impact.

2. Determine the level of significant (\( \alpha \))
   In this case, the level of significant is 5% with the level of confidence 95%

3. Determine the testing criteria
   \( H_{01}, H_{02}, H_{03}, H_{04}, H_{05} \) are not accepted if : t-test > t-table or -t-test < -t-table.
$H_{01}, H_{02}, H_{03}, H_{04}, H_{05}$ are accepted if $-t_{table} \leq t_{test} \leq t_{table}$

4. Conclusion
   a) If $H_{01}$ not accepted so the lost of housing as partial not have correlation to economic impact.
      If $H_{01}$ accepted so the lost of housing have correlation to economic impact.
   b) If $H_{02}$ not accepted so the lost of infrastructure not have correlation to economic impact.
      If $H_{02}$ accepted so the lost of infrastructure have correlation to economic impact.
   c) If $H_{03}$ not accepted so the social criteria not have correlation to economic impact.
      If $H_{03}$ accepted so the social criteria have correlation to economic impact.
   d) If $H_{04}$ not accepted so the lost of economic not have correlation to economic impact.
      If $H_{04}$ accepted so the lost of economic have correlation to economic impact.
   e) If $H_{05}$ not accepted so cross sector not have correlation to economic impact.
      If $H_{05}$ accepted so cross sector have correlation to economic impact.

2.3.3 Normality assumption test

Normality test aims to measure the data having the normal distribution so be able to use on parametric statistic. In this case, Kolmogorov-Smirnov test used to determine the normal distribution from data. If the probability $> 0.05$ so the data is normal distribution and if probability $\leq 0.05$ the data is not normal distribution instead.

3. Results and Discussion
To know the economic impact, the data using the total economic loss ($Y$) which consist in 5 variable there are 1. The loss of housing 39.318% ($X_1$), 2. Loss of infrastructure 15.477% ($X_2$), 3. Social 4.779% ($X_3$), 4. Economic source 7.021% ($X_4$), 5. Cross sector such as banking and living environment 33.405% ($X_5$). Those data will generated into 50 data using Normal Distribution with 1% standard deviation from original data.

3.1 Significance Test ($F$ statistics test)

After the data convert to logarithm natural and processed with the $F$ test, the result is

| Table 1 ANOVA table which show the F-test value |
|-----------------------------------------------|
| $df$ | $SS$     | $MS$     | $F$         | $Significance F$   |
|------|----------|----------|-------------|-------------------|
| Regression | 5 | 0.000836 | 0.000167 | 2.767859 | 0.029363274 |
| Residual   | 44 | 0.002659 | 6.04E-05 | 0.003495 |
| Total      | 49 |           |            |                  |

Based on the table of ANOVA showed that $F$-test 2.767859 > $F$-table 2.42 and the value of significance $> 0.05 (\alpha)$, so the conclusion is $H_0$ not accepted that means the lost of housing, lost of infrastructure, lost of social criteria, lost of economic source and lost of cross sector simultaneous have a correlation into the economic impact.

3.2 Wald Test ($t$ test)

After the data convert to logarithm natural and processed with the $t$ test, the result is
Table 2 Table which show the value of t-test

|               | Coefficients | Standard Error | t Stat  |
|---------------|--------------|----------------|---------|
| Intercept     | 26,96087815  | 5,463150823    | 4,93504189 |
| Lost of Housing| -0,02969591  | 0,098459932    | -0,301604  |
| Lost of Infrastructure| -0,230823501 | 0,124361944    | -1,85606219 |
| Lost in Social | -0,15389522  | 0,113426691    | -1,35678136 |
| Lost of Economic| 0,244718139  | 0,110096817    | 2,22275398  |
| Lost in Cross Sector| 0,176663318  | 0,107127912    | 1,64908766  |

a) First hypothesis
The value of t-test -0.30160 > t-table -1.68 so other lost of housing have correlation to economic impact.

b) Second hypothesis
The value of t-test -1.85606219 < t-table -1.68 so the lost of infrastructure not have correlation to economic impact.

c) Third hypothesis
The value of t-test -1.35678136 > t-table -1.68 so the social criteria have correlation to economic impact.

d) Fourth hypothesis
The value of t-test 2.22275398 > t-table 1.68 so the lost of economic have correlation to economic impact.

e) Fifth hypothesis
The value of t-test 1.64908766 < t-table 1.68 so cross sector have no correlation to economic impact.

3.3 Normality assumption test
After the data convert to logarithm natural and processed with the normality assumption test, the result is

![Normality assumption test](image1.png)

Figure 1. Normality assumption test
The value of KS 0.084 and the P-Value > 0.150 which mean bigger than 0.05 (α) so the variable determined as a normal distribution.

3.4 Partial Least Square Method

The 50 data changed into the Ln data to follow Cobb-Douglas function. After all data processed by PLS the result is
Constant = 26.9609, \( X_1 = -0.0297 \), \( X_2 = -0.2308 \), \( X_3 = -0.1539 \), \( X_4 = 0.2447 \), \( X_5 = 0.1767 \)

3.5 Cobb-Douglas Method

so the regression result followed Cobb-Douglas Function (2)
\[
\ln Y = \ln 26.9609 - 0.0297 \ln X_1 - 0.2308 \ln X_2 - 0.1539 \ln X_3 + 0.2447 \ln X_4 + 0.1767 \ln X_5
\]

and can be written as (1)
\[
Y = 511.647 \times 0.0001 \times X_1^{-0.0297} \times X_2^{-0.2308} \times X_3^{-0.1539} \times X_4^{0.2447} \times X_5^{0.1767}
\]

4. Conclusion

The model solution in the economic impact due to Cimanuk river flood impact was created by Cobb-Douglas Method after the constant got by Partial Least Square Method. From the result of the discussions, it can be conclude that The Cobb-Douglas Method be able to forming the mathematical model of the flood depend on the data of the economic lost. And the mathematical model can be used by government to make the regulation to anticipate the flood.

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