METHOD OF THE FINITE-ELEMENT MODEL FORMATION CONTAINING THE 3D ELEMENTS FOR STRUCTURAL CALCULATIONS OF THE REINFORCED CONCRETE STRUCTURES CONSIDERING THE CRACK OPENING

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Resume
This article presents the 3D computational modeling method for reinforced concrete structures. An example of calculation of the reinforced concrete beam, using the Finite Element Method in SCAD++ following proposed algorithm, is given. Results comparison to the analytical calculation of the model with selected reinforcement is presented. For concrete, the 3D solid Finite Elements are used and the 3D beam elements for reinforcement. The model is formed using AutoCAD and AutoLISP, which creates a text data file in SCAD format for the description of model. In addition, computation of the 3D model of the crossbar with a crack is performed. Crack sizes are set in the stretched zone based on data from initial calculation. Graphic results obtained in SCAD++ are presented.

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1 Introduction

The reinforced concrete (RC) structures can have various applications in construction, such as beams, slabs, shells, massive structures, often of a complex shape, defined by the architectural features of the designed structure and construction process. The reinforced concrete structures calculation, based on standard approaches, does not define an adequate model for the stress-strain state, both in concrete and in reinforcement due to multiple reasons, such as crack propagation in concrete, complex geometry and structural dimensions, not allowing the use of beam theory.

Currently, engineers use the rod elements for calculations of the reinforced concrete structures, as a creation of volumetric elements and complex shape, is a very difficult and time-consuming process. Appearance of cracks is allowed by standards [1]. However, as shown in results of simulation performed in this article, appearance of even minor cracks noticeably increases stresses in the reinforcement rebars. Such consequences cannot be considered in calculations without using the 3D elements.

Calculation of the crack formation and size of the crack opening is important to ensure the bearing capacity of the reinforcement and durability of the reinforced concrete structures. The paper [1] presents a comparative analysis of the existing SP calculation methods for the normal crack formation, based on a nonlinear deformation model. For simple types of structures, the joint venture allows calculation according to a simplified method (by limiting forces). Usually, an assumption to perform calculations, using simplified methods, is organized in such a way that the obtained results provide a margin of reliability. However, that is not valid in the case of the normal crack opening width analysis, as shown in the article [1].

Remaining within the same normative document, the spread of acceptable crack opening values can exceed 50 % [1].

If one considers problems with reinforcement in a compressed zone and stronger concrete, the discrepancies between the deformation and force approach can increase up to 200 - 300 % [1].

As a result, it can be concluded that in order to solve the described problem, the development of methodology that allows to determine as accurately as possible the value of crack opening in reinforced concrete structures is needed.

The purpose of this article is to present a method of a complex strength calculation of reinforced concrete elements, allowing to consider the factors mentioned above and to obtain more precise values of the elements stress-strain state, including reinforcement, considering...
1. SCAD provides data exchange with other programs using:
   • universal formats (IFC, CIS/2, DXF, DWG, TXT);
   • data formats of Advance Steel, ANSYS, STAAD, Abaqus, Femap, GMSH, NetGen;
   • plugins for Revit, ArchiCAD, Tekla.

2. AutoCAD software to define a beam reinforcing frame of RC models, networks in the foundation of solid 3D models and their nodal coordinates using AutoCAD graphic database.

3. Program, developed by S. N. Nazarenko using AutoLISP language, embedded in AutoCAD, which is also described in the article [18], automatically creating a text data file in SCAD format [18-19] for a FE model, consisting of 3D FEs. This program automatically generates arrays of topology and coordinates for the finite element model, then generates text data file in SCAD format for definition of the 3D model sub-structures. Volumetric sub-structures are then joined together, merging with the core elements in SCAD++ assembly procedure, as well. More details about program realization on AutoLISP for formation of covers are also available in [2, 18-19]. Problems of modeling and calculating massive structures of bridges, supports and other 3D structures, based on their parametric dimensions, were solved by this program. Using this program in conjunction with AutoCAD allows optimizing SCAD 3D modeling of structures and reducing time consumed.

### Example

The developed method is demonstrated using an example of the reinforced concrete beam with rectangular cross-section. It should be mentioned that the proposed method can be used for calculation of the reinforced concrete structures with more complex cross-sections, as well.
For the girder shown in Figure 1, calculation is done in system SCAD++ for the purpose of the subsequent comparison of results for two models:

The first model: the beam model, results of deflection determination for this model are shown in Figure 3;

The second model: the 3D model formed by solid 3D finite elements used for concrete, which were combined in SCAD++ by means of assembly with beam elements simulating reinforcement. The process of forming the 3D model of the girder is shown in Figures 4-6. Results of its calculation are shown in Figures 7-14.

4 Standard method

At the first step, the calculation of the girder is performed and modeling it with the rod elements, using the standard methodology described in SP [20-22].

Selection of reinforcement was carried out by SP 63.133.30.2012.

The following parameters were used:
• element type - bendable beam element;
• load case - uniaxial bending;
• maximum reinforcement percentage - 10%.

Longitudinal reinforcement of class A400 steel rebars and transverse reinforcement of class A240 steel rebars were used for calculation. Concrete working conditions ratio 1 was applied.

For the concrete, the parameters specified in Table 1 were used.

By iteration and meeting the above conditions, the maximum value of crack opening, equal to 0.388 mm, is obtained.
After obtaining the stress-strain state and cracks opening by the standard method, following are the stages of formation and calculation of the 3D model of a beam with application of the 3D solid FE and crack modeling, using axial symmetry for a beam from Figure 1, what reduces the number of FE twice. We use the AutoCAD software. The cross-section in the middle of the beam is given in Figure 4. For formation of model of the 3D FE, it is necessary values of factor of reduction of armature to concrete, in corresponding formulas:

- $h_0$ - operational height;
- $y_c$ - for bending elements $y_c = x$, where $x$ is the height of the compressed concrete zone.
- $\alpha_{sc}$ - coefficient of adduction.

According to SP, the following options can be applied:

- The coefficient $\psi_s = 1 - 0.8 \frac{\alpha_{sc,ov}}{\alpha_{so}}$ or $\psi_s = 1 - 0.8 \frac{M_{crv}}{M}$
- Crack initiation moment $M_{crv} = 1.3 R_{t,crv} W_{red}$ ($W_{red}$ defined with or without assuming the reinforcement);
- Stress $\sigma_s = \frac{M(h_0 - y_c)}{I_{red}} \alpha_{sc}$ or $\sigma_s = \frac{M}{z_e A_S}$
- the distance from the center of gravity of the stretched rebars to the point of application of resulting force in the compressed zone of the element $z_e = h_0 - \frac{x}{3}$ or $z_e = 0.8h_0$.

Similarly, $\sigma_{sc,ov}$ - tension in the longitudinal stretched reinforcement in the section with a crack immediately after the formation of normal cracks.

### 5 New method

After obtaining the stress-strain state and cracks opening by the standard method, following are the stages of formation and calculation of the 3D model of a beam with application of the 3D solid FE and crack modeling, using axial symmetry for a beam from Figure 1, what reduces the number of FE twice. We use the AutoCAD software. The cross-section in the middle of the beam is given in Figure 4. For formation of model of the 3D FE, it is necessary
Dimensions of the 3D finite elements would be close to the topological cube, which gives better accuracy of calculations in the FEM procedures.

In other possible cases of modeling reinforced concrete structures with more irregular placement of the transverse rebars than in this example, additional 3D sub-structures by length can be introduced, which can be grouped into separate parts that are joined during the assembly in SCAD.

Further, each separate sub-network, shown in Figure 4, by dismembering of an initial network by a command AutoCAD, is filled with primitives 3DFACE. The program AutoLISP, forming the text description of each sub-structure, is started. The resulting sub-structure is then uploaded into SCAD and saved as a separate SCAD project file. Then, it is proceeded to the final assembly of the model from 3D parts of the structure modeling concrete. The description of this process can be found in the article [18]. Result of an assembly for this example, is presented in Figure 5. For the created model, it is possible to set in SCAD the missing calculation components such as rigidity of 3D elements, units with support, load, before the further final assembly with the substructure modeling the reinforcement.

To simulate the rebar, the AutoCAD LOCK and MASSIVE commands were initially used. To make the nodes of 3D beam (AutoCAD segments) and the nodes of the 3D solid elements coincide, the MASSIVE command is used (Figure 6). Then, after receiving the two files of the AutoCAD drawing with the segments simulating longitudinal and transverse rebars, they are exported to SCAD in DXF format for the subsequent assemblage with substructure (Figure 5), simulating concrete. Each of the two drawings...
of the reinforcement, longitudinal and transverse, in order to facilitate the task of rigidity definition in SCAD, is exported separately, then combined with the model of concrete in the assembly procedures in SCAD.

6 Results

Some results of calculation in SCAD for the 3D model of the concrete beam, combined in assemblage with steel rebars, are shown in Figures 7-10.

The maximum value of displacement in the Z-axis direction, obtained in the model calculation, is equal to \(-3.87 \times 10^{-3}\) m, or 0.05 mm in the downwards direction. The comparative analysis of difference in deflection values of the beam (calculated numerically) and 3D model gave 0.05 mm or 1.25%. The smaller deflection value obtained for the 3D model in comparison to the beam model can be explained by considering the rigidity of the transverse rebar and more accurate distribution of rigidity in the volume of the 3D model compared to the beam theory.

In Figure 7 are also shown the fixed nodes and the axial load (Figure 1), distributed along the transverse line of symmetry in the upper part.

Figures 8 and 9 display the load replacing the concentrated force shown in Figure 1 with calculated force values, considering the symmetry and the unequal spacing between the units, applied to the concrete. The table allows to determine the height of the stretched zone in the critical cross-section along the axis of symmetry of the girder with the maximal internal forces (right-hand end with the applied load).
After obtaining the precise stress-strain state using the 3D solid FE for the concrete modeling and beam FE for the reinforcement, it is proceeded to the cracks modeling and their opening determination.

Then, it is proceeded to modeling of a crack located in the most loaded cross-section, along the axis of symmetry.

In determining the stress-strain state, the plot of the tangential stress $\tau_{xz}$ distribution can be of interest. In comparison to the theoretical formulas of materials resistance, a significant difference between the $\tau_{xz}$ plot and the picture shown in Figure 9, is obtained, which can be explained by influence of the transverse reinforcement.

After obtaining the precise stress-strain state using the 3D solid FE for the concrete modeling and beam FE for the reinforcement, it is proceeded to the cracks modeling and their opening determination.

In Figure 8 SCAD stress isofields of $\sigma_x$ in the direction of the longitudinal axis X on a 3D model.

In Figure 9 Isofields and isolines of tangential stresses $\tau_{xz}$ in the model.
of the reinforced concrete beam (see Figures 8, 10). The height of a crack development is determined by stress $\sigma_x$ isopolls preliminary calculated in SCAD++. In Figure 10, obtained based on the calculation results, coloring of the model in a compressed and compressed-strained zone is disabled by means of SCAD++. The stretched zone of the structure, in the right cross section, as it follows from Figure 8, extends to the middle of the section height.

The crack is modeled by removing the longitudinal connections at the right-hand end of the beam, along the symmetry axis, to the height of the lower half of cross-section. In this case, appearance of a crack in this section...
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Figure 12 Relation between the maximum crack opening value $d_c$ and crack height $h_c$.

Figure 13 Diagrams of longitudinal forces $N$ in the reinforcement rebars of the calculated RC structure with a crack.

will lead to displacement of the lower edge to the left, because this accepted section with the crack is located in the symmetry plane. The calculation of this structure is performed.

As a result of the structure calculation, with a modeled crack, the obtained value of maximum deflection - displacement in the Z-axis, has increased by 11.9 %, up to - 4.33 mm.

Some other calculation results in SCAD++ 3D model with a crack are shown in Figures 11 and 12. Longitudinal movements in the section along the axis of symmetry of the beam - opening of the assumed crack, are shown in Figure 11.

Figure 11 also shows regions in the area of the bottom longitudinal rebars, painted grey, with zero displacement along the X axis due to longitudinal bonds defined in these nodes. The connections in the assumed stretched area are also shown in the form of rectangles above the cross-section. The maximum value of the crack opening as given in the table in Figure 11, is: $0.0563 \times 2 = 0.113$ mm (multiplied by 2 assuming displacements in the symmetrical part of structure). Six calculations were performed, with longitudinal connections with the assumed crack being removed on one row above at each of the subsequent steps.

The graph of the $d_c$ maximum crack opening values variation, obtained in calculation for each stage of crack development, is presented in Figure 12.

The longitudinal forces $N$ in the reinforcement rebars in the cross section with a crack have increased significantly compared to the calculated values obtained in calculation of the beam without a crack. The N-plots in rebar are shown in two views in Figure 13 with the table of values $N$, also the fixation points are indicated.

It should be noted that the location of cracks in the proposed 3D model of reinforced concrete structures, their length and direction of development, require additional theoretical and experimental justification. Cracks can also be simulated by dividing in SCAD++ the neighboring bulk finite elements by their contact boundaries.
The two models’ calculations results were compared by the crack opening values: 0.388 mm according to the standard method and its maximum value 0.138 mm obtained from the 3D model calculation.

Results of the modeling were compared to results obtained by the method established in [22], which is based on stochastic and probabilistic approaches for the characteristics of reinforcement and concrete and is confirmed by extensive practical tests [23-24]. The characteristics used in the calculations with 95% probability will not exceed the characteristics in real constructions. Safety factors are applied. Thus, this technique provides a guarantee that the results obtained from it will not exceed the critical values included in the SP [22]. According to the standards for this type of construction and operating conditions, the crack opening value should not exceed 0.4 mm [22]. The crack growth to a compressed zone (opening width 0.1126 mm) and then to the moment when the crack stopped (0.138 mm), is simulated. Multiple cracks were modeled, at each stage, the crack opening value was fixed and the most dangerous crack was selected (Figure 12). At the maximum length of the crack, the opening value was 0.138 mm. This corresponds to the criterion defined by standards and is less than those obtained using the method mentioned above [20-22].

The results obtained are less than those calculated according to the standard method, possibly due to the fact that the model took into account the volume work of concrete, longitudinal reinforcement in the compressed and stretched part of the structure, transverse reinforcement.

Results of the two models’ calculations are compared according to the crack opening values: 0.388 mm according to the standard method and 0.1126 mm obtained from the 3D model calculation. These results showed that the obtained value of the crack opening is more than 3 times less than calculated according to the norms, which may be due to the fact that the model that was built took into account the volume action of concrete, longitudinal reinforcement in the compressed and stretched part of the structure, transverse reinforcement.

7 Conclusions

Result of the work, presented in this article, is development of methods for formation of the 3D finite element models of reinforced concrete structures with use of the bulk finite elements for the modeling of concrete and rod elements, modeling rebar, allowing strength calculation of reinforced concrete beams, taking into account crack opening. This applies not only to beam structures, but to the reinforced concrete structures almost of any shape, as well. The proposed method allows modeling cracks in concrete and obtaining the values of crack opening considering the work of longitudinal reinforcement located in a stretched and compressed zone of the structure, transverse reinforcement, which cannot be done using the existing standards. The stress-strain state parameters, obtained by the precise model, allow optimization reinforcement parameters, analyze and consider stress concentrators with possible reinforcement and reinforcement of non-standard cross-sections. Developed program, applied in this article, can be also applied into another FEM software supporting the corresponding file exchange formats. It allows to optimize as much as possible the process of modeling of the massive reinforced concrete structures and thus to reduce time costs.

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