Ginzburg-Landau approach to the three flavor LOFF phase of QCD

R. Casalbuoni
Dipartimento di Fisica, Università di Firenze, I-50019 Firenze, Italia and
I.N.F.N., Sezione di Firenze, I-50019 Firenze, Italia

R. Gatto
Départ. de Physique Théorique, Université de Genève, CH-1211 Genève 4, Suisse

N. Ippolito, G. Nardulli, and M. Ruggieri
Università di Bari, I-70126 Bari, Italia and
I.N.F.N., Sezione di Bari, I-70126 Bari, Italia

(Dated: August 25, 2018)

We explore, using a Ginzburg-Landau expansion of the free energy, the Larkin-Ovchinnikov-Fulde-Ferrell (LOFF) phase of QCD with three flavors, using the NJL four-fermion coupling to mimic gluon interactions. We find that, below the point where the QCD homogeneous superconductive phases should give way to the normal phase, Cooper condensation of the pairs $u - s$ and $d - u$ is possible, but in the form of the inhomogeneous LOFF pairing.

PACS numbers: 12.38.Aw, 12.38.Lg

I. INTRODUCTION

At high quark density and small temperatures Quantum-Chromo-Dynamics (QCD) predicts Cooper pairing of quarks due to the existence of an attractive quark interaction in the color antisymmetric channel, see [1, 2, 3] and for reviews [4, 5]. At extreme densities the energetically favored phase is the Color-Flavor-Locking (CFL) phase, characterized by a spin 0 diquark condensate antisymmetric in both color and flavor [6]; at intermediate densities the situation is much more involved, because one cannot neglect the strange quark mass and the differences $\delta \mu$ in the quark chemical potentials induced by $\beta$ equilibrium. Several ground states have been considered in the literature, from the 2SC phase [2], to the gapless phases $g_{2SC}$ [7] and $g_{CFL}$ [8, 9]. The gapless phases are instable as shown by imaginary gluon Meissner masses (for $g_{2SC}$ see [10], for $g_{CFL}$ see [11] and [12]). This seems to be connected to the existence of gapless modes in these phases [13]. An instability is present also in the 2SC phase [10]. Though this phase has no gapless mode, imaginary gluon masses are present when the gap $\Delta$ and $\delta \mu$ satisfy the condition

$$\frac{\Delta}{\sqrt{2}} \leq \delta \mu \leq \Delta.$$  

Another superconductive state discussed in the literature is the Larkin-Ovchinnikov-Fulde-Ferrell (LOFF) [14] phase. The relevance of this phase is based on the possibility that, for appropriate values of $\delta \mu$, it can be advantageous for quarks to form pairs with non-vanishing total momentum: $p_1 + p_2 = 2q \neq 0$, see [15, 16] and for a review [17]. As far as instability is concerned, the authors in [15] have shown that, with two flavors, the instability of 2SC implies that the LOFF phase is energetically favored. Moreover, in the LOFF phase with two flavors the gluon Meissner masses are real [19].

Thus far only the case of two species for the LOFF phase has been studied. This is not justified in QCD. At intermediate densities all the three quarks: $u$, $d$ and $s$ should be considered. The three flavor problem is however much more involved and difficult to work out. We present here a first attempt to study the three flavor LOFF phase of QCD. Our approach is based on a Ginzburg-Landau (GL) expansion of the free energy. Differently from the CFL phase, where quark matter is in $\beta$ equilibrium while being also electrically and color neutral, here we should impose these conditions. We shall consider in the sequel only $\beta$-equilibrated and electrically neutral quark matter, while assuming that the color-chemical potentials vanish. This is an approximation we discuss below.

II. GAP EQUATION

To get the gap equation in the Ginzburg Landau approximation, we start with the Lagrangean density for three flavor ungapped quarks:

$$\mathcal{L} = \bar{\psi}_{i\alpha} \left(i D_{i\alpha}^{\alpha\beta} - M_{ij}^{\alpha\beta} + \mu_{ij}^{\alpha\beta} \gamma_5 \right) \psi_{j\beta}.$$  \hspace{1cm} (1)

$M_{ij}^{\alpha\beta} = \delta^{\alpha\beta} \text{diag}(0, 0, M_s)$ is the mass matrix and $D_{ij}^{\alpha\beta} = \delta^{\alpha\beta} \delta_{ij} + igA_a T^{\alpha\beta}_{ij} \delta_{ij}$; $\mu_{ij}^{\alpha\beta}$ is a diagonal color-flavor matrix depending in general on $\mu$ (the average quark chemical potential), $\mu_e$ (the electron chemical potential), and $\mu_3$, $\mu_8$, 

...
related to color. We do not require color neutrality and we work in the approximation $\mu_3 = \mu_8 = 0$, which might be justified by the results of Ref. 3 for the gCFL phase showing that $\mu_3$ and $\mu_8$ assume in general small values (at least in the region of interest, see later). Therefore in this paper

$$\mu^{\alpha\beta}_{ij} = (\mu \delta_{ij} - \mu_s Q_{ij}) \delta^{\alpha\beta} = \mu_i \delta_{ij} \delta^{\alpha\beta},$$

(2)

where $Q$ is the quark electric-charge matrix.

We treat the strange quark mass at the leading order in the $1/\mu$ expansion; this corresponds to a shift in the chemical potential of the $s$ quark: $\mu_s \to \mu_s - \frac{M_s^2}{2\mu}$. This is the same approximation used in Refs. 3, 11 for the study of the gCFL phase. Therefore:

$$\mu_u = \mu - \frac{2}{3} \mu_e, \quad \mu_d = \mu + \frac{1}{3} \mu_e, \quad \mu_s = \mu + \frac{1}{3} \mu_e - \frac{M_s^2}{2\mu}.$$  

(3)

Another approximation we employ is the High Density Effective Theory (HDET), see 20, 21, 22 and, for a review, 3. Here one decomposes the quark momentum into a large component, proportional to $\mu$, and a residual small component: $p = \mu n + \ell$; $n$ is a unit vector and $\ell$ is the small residual momentum. Moreover one introduces $n$-dependent fields $\psi_n$ and $\Psi_n$ by the Fourier decomposition

$$\psi(x) = \int \frac{dn}{4\pi} e^{i\mu n \cdot x} (\psi_n(x) + \Psi_n(x));$$

(4)

$\psi_n$ and $\Psi_n$ correspond to positive and negative energy solutions of the Dirac equation. Substituting the expression 4 in the Eq. 2 one gets at the leading order in $1/\mu$

$$L = \int \frac{dn}{4\pi} \psi_{n,\alpha}^\dagger \left( iV \cdot D^\alpha_{ij} + \tilde{\mu}_i \delta^\alpha_{ij} \delta_{ij} \right) \psi_{n,\beta},$$

(5)

where $V^\mu = (1, \mathbf{n})$, $\tilde{V}^\mu = (1, -\mathbf{n})$ and $\tilde{\mu}_i = \mu_i - \mu$.

It is convenient to change the basis for the spinor fields by defining $\psi_A = (\psi_{sr}, \psi_{sb}, \psi_{dr}, \psi_{db}, \psi_{ur}, \psi_{ub}, \psi_{sr}, \psi_{db})$. This change of basis is performed by unitary matrices $F_A$, whose explicit expression can be found in Ref. 11. To the Lagrangean in Eq. 3 we add a Nambu-Jona Lasinio four fermion coupling treated in the mean field approximation. This corresponds to the same coupling and the same approximation used in Ref. 3. The gap term in the resulting Lagrangean is conveniently treated by introducing the Nambu-Gorkov field

$$\chi_A = \frac{1}{\sqrt{2}} \left( \begin{array}{c} \psi_n \\ C \psi^*_{-n} \end{array} \right)_A,$$

(6)

so that the Lagrangean reads

$$L = \frac{1}{2} \sum_{A,B} \int \frac{dn}{4\pi} \int dE d\xi \frac{1}{(2\pi)^2} \chi_A^\dagger \left( \begin{array}{cc} (E - \xi + \tilde{\mu}_A) \delta_{AB} & -\Delta_{AB}(r) \\ -\Delta^*_{AB}(r) & (E + \xi - \tilde{\mu}_A) \delta_{AB} \end{array} \right) \chi_B,$$

(7)

where $E$ is the energy, $\xi = \ell \cdot \mathbf{n}$ is the component of the residual momentum along $\mathbf{n}$ and satisfies: $|\xi| < \delta$, with $\delta$ an ultraviolet cutoff. Moreover $(\tilde{\mu})_A = (\tilde{\mu}_u, \tilde{\mu}_d, \tilde{\mu}_s, \tilde{\mu}_d, \tilde{\mu}_u, \tilde{\mu}_s, \tilde{\mu}_u, \tilde{\mu}_d)$.

We assume the pairing ansatz

$$< \psi_{i\alpha} C \gamma_5 \psi_{j\beta} >= \sum_{I=1}^{3} \Delta_I(r) \epsilon^{\alpha\beta} \epsilon_{ijI},$$

(8)

with

$$\Delta_I(r) = \Delta_I \exp (2i q_I \cdot r).$$

(9)

In other words, for each inhomogeneous pairing we assume a Fulde-Ferrell ansatz; $2q_I$ represents the momentum of the Cooper pair. The gap matrix $\Delta_{AB}$ in 7 can be expressed in terms of the three independent functions $\Delta_1(r)$, $\Delta_2(r)$, $\Delta_3(r)$ describing respectively $d-s$, $u-s$ and $u-d$ pairing. The explicit expression of $\Delta_{AB}$ can be found in 3, 11.
To write down the gap equation it is useful to introduce the following components of the free quark propagator

\[
[S_{0}^{11}]_{AB} = \frac{\delta^{AB}}{E - \xi + \bar{\mu}_{A}}, \quad [S_{0}^{22}]_{AB} = \frac{\delta^{AB}}{E + \xi - \bar{\mu}_{A}}.
\]  

(10)

The quark propagator is the matrix

\[
S_{AB} = \begin{pmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{pmatrix}_{AB}
\]

whose components satisfy the Gorkov equations

\[
S_{11} = S_{0}^{11} + S_{0}^{11} \Delta(r) S_{21}, \quad S_{21} = S_{0}^{22} \Delta^{*}(r) S_{11}.
\]

(12)

\(S_{21}\) is the anomalous propagator involved in the gap equation.

The wave vectors \(q\) should be derived by minimizing the free energy. We will fix the norms \(|q|\) by a minimization procedure. As to their directions, we will limit the analysis to four structures, choosing among them the one with the smallest value of the energy. The first structure has all \(q\) along the positive \(z\)–axis. The structures 2, 3, 4 have, respectively, \(q_{1}, q_{2}, q_{3}\) along the positive \(z\)–axis (the remaining two momenta along the negative \(z\)–axis). This is obviously a limitation. It is justified by our final results that show the existence of a range of values of the strange quark mass where the LOFF phase, even with these limitations, is favored in comparison with other QCD phases.

The gap equation in the HDET formalism can be written as follows:

\[
\Delta^{s}_{AB}(r) = i 3 G V^{\mu} V^{\nu} \sum_{C,D=1}^{9} h_{\alpha C}^{*} h_{DB}^{*} \int \frac{d \mathbf{n}}{4 \pi} \int \frac{d^{3} \ell}{(2 \pi)^{3}} \int \frac{dE}{2 \pi} S_{21}(E, \ell)_{CD} g_{\mu \nu} \delta_{ab},
\]

(13)

where \(S_{21}\) is given in Eq. (12); in the above equation \(h_{DB}^{*}\) is a Clebsch-Gordan coefficient. It is expressed by the formula \(h_{DB}^{*} = \text{Tr}[F_{D}^{\dagger} T_{B} F_{B}^{*}]\) in terms of the unitary matrices \(F_{A}\) used to write the quark fields as in Eq. (10), i.e. in the basis \(A = 1, \ldots, 9\). \(G\) is the Nambu-Jona Lasinio coupling constant, of dimension mass \(-2\). In what follows, we shall get rid of \(G\) introducing the value of the CFL gap parameter \(\Delta_{0}\) as a measure of the strength of the interaction (see below, Eq. (18)).

III. GINZBURG-LANDAU EXPANSION

Performing the Ginzburg-Landau expansion of the propagator

\[
S_{21} = S_{0}^{22} \Delta^{*} S_{0}^{11} + S_{0}^{22} \Delta^{*} S_{0}^{11} \Delta S_{0}^{22} \Delta^{*} S_{0}^{11} + O(\Delta^{5})
\]

(14)

we get

\[
\Delta_{I} = \Pi_{I} \Delta_{I} + \sum_{J \neq I} J_{I,J} \Delta_{J}^{2} + O(\Delta^{5}), \quad I = 1, 2, 3.
\]

(15)

Let us comment on the functions \(\Pi_{I}\) and \(J_{I,J}\) appearing in this expansion. \(\Pi_{I}\) are defined as follows: \(\Pi_{1} = \Pi(q_{1}, \delta \mu_{ds})\), \(\Pi_{2} = \Pi(q_{2}, \delta \mu_{us})\), \(\Pi_{3} = \Pi(q_{3}, \delta \mu_{ud})\), with

\[
\delta \mu_{ud} = \frac{\bar{\mu}_{d} - \bar{\mu}_{u}}{2} - \frac{\bar{\mu}_{s}}{2}, \quad \delta \mu_{us} = \frac{\bar{\mu}_{s} - \bar{\mu}_{u}}{2} - \frac{\mu_{s} - M_{t}^{2}}{4 \bar{\mu}} , \quad \delta \mu_{ds} = \frac{\bar{\mu}_{d} - \bar{\mu}_{s}}{2} = -\frac{M_{d}^{2}}{4 \bar{\mu}}.
\]

(16)

and

\[
\Pi(q, \delta \mu) = 1 + \frac{2 G \mu^{2}}{\pi^{2}} \left(1 - \frac{\delta \mu}{2 q} \log \frac{|q + \delta \mu|}{|q - \delta \mu|} - \frac{1}{2} \log \left|\frac{4(q^{2} - \delta \mu^{2})}{\Delta_{0}^{2}}\right|\right).
\]

(17)

We note that \(\Pi\) is analogous to the function determining the behavior of the free energy in the GL approximation of the LOFF phase with two flavors. We have introduced the parameter \(\Delta_{0}\) to get rid of the ultraviolet cutoff \(\delta\). It is defined by

\[
\Delta_{0} = 2 \delta \exp \left(-\frac{\pi^{2}}{2 G \mu^{2}}\right).
\]

(18)
Δ0 is equal to the CFL gap for Ms = 0 and με = 0 in the weak coupling limit, with no sextet condensation. As for J_{1J}, we have, for the diagonal components: J_{11} ≡ J_1 ≡ J(q_1, δμ_ds), J_{22} ≡ J_2 ≡ J(q_2, δμ_us), J_{33} ≡ J_3 ≡ J(q_3, δμ_ud), with

\[ J(q, δμ) = -\frac{Gμ^2}{2π^2} \frac{1}{q^2 - δμ^2} \, . \] (19)

The off-diagonal term J_{12} is

\[ J_{12} = \frac{Gμ^2}{π^2} \int \frac{d n}{4π} \frac{1}{(2q_1 \cdot n + μ_s - μ_d - iε)(2q_2 \cdot n + μ_s - μ_u - iε)} \, . \] (20)

J_{13} is obtained from J_{12} in (20) by the exchange q_2 → q_3 and μ_s ↔ μ_d; J_{23} from J_{12} by q_1 → q_3 and μ_s ↔ μ_u.

### IV. FREE ENERGY

Let us now consider the free energy Ω. It is obtained by integrating the gap equation. The result is

\[ Ω = Ω_n + \sum_{I=1}^{3} \left( \frac{α_I}{2} Δ^2_I + \frac{β_I}{4} Δ^4_I + \sum_{J≠I} β_{IJ} Δ^2_I Δ^2_J \right) + O(Δ^6) \] (21)

with

\[ Ω_n = -\frac{3}{12π^2} \left( μ^4_u + μ^4_d + μ^4_s \right) - \frac{μ^4_e}{12π^2} \] (22)

where the chemical potentials for quarks are defined in Eq. (3) and the coefficients are given by

\[ α_I = \frac{2 (1 - Π_I)}{G} \, , \quad β_I = -\frac{2 J_I}{G} \, , \quad β_{IJ} = -\frac{2 J_{IJ}}{G} \] (23)

Electric neutrality is obtained by imposing the condition

\[ -\frac{∂Ω}{∂μ_e} = 0 \, , \] (24)

which, together with the gap equations, gives, for each value of the strange quark mass, the electron chemical potential μ_e and the gap parameters Δ_I. Moreover one should determine q_I by searching for the energetically favored solution. This is a complex task as it would require the simultaneous solution of the previous equations (24) and (15) together with:

\[ 0 = \frac{∂Ω}{∂q_I} = Δ_I \frac{∂α_I}{∂q_I} + Δ_I \sum_{J=1}^{3} Δ_J \frac{∂β_{IJ}}{∂q_I} \, , \quad I = 1, 2, 3 \, . \] (25)

Moreover one should look for the most energetically favored orientations of the three vectors q_I in space. A complete analysis is postponed to a future paper; as discussed above we have limited the analysis to the four structures characterized by all vectors q_I parallel or antiparallel to the same axis. Even with this limitation we are able to prove that there exists a window of values of Ms where the LOFF phase is favored in comparison with other phases of QCD, as it will be seen below. As to the norms |q_I|, since we work in the GL approximation, we can neglect the O(Δ^2) terms in (25). As a consequence we simply get \( \frac{∂α_I}{∂q_I} = 0 \), which, being identical to the condition for two flavors, gives the result q_I = 1.1997|δμ_I| [14, 15].

### V. RESULTS AND DISCUSSION

Our results are summarized in Figs. [1-4]. In Fig. [1] we give Ω_{LOFF} − Ω_{norm} (in units 10^6 MeV^4) as a function of M^2_s/μ (in MeV).
We report only the energetically favored solution. It corresponds to $\Delta_1 = 0, \Delta_2 = \Delta_3$ and $q_2, q_3$ parallel (structure 1, which is identical in this case to the structure 2). We do not report the other solutions corresponding to local minima of $\Omega$. We also found a solution with $\Delta_1 \neq 0$ and $\Delta_2 \neq \Delta_3$ but it can only exist in a kinematical range where the LOFF phase is energetically disfavored in comparison with the CFL or the gCFL phases. The structures 3 and 4 ($q_2, q_3$ antiparallel) have almost vanishing gaps and correspond only to local minima of the free energy. The results in this figure and in the subsequent ones are obtained for $\mu = 500$ MeV (for $\mu = 400$ MeV the results are qualitatively similar). The value of the CFL gap for zero strange quark mass is fixed at $\Delta_0 = 25$ MeV. This is the same value used in Ref. [9]. This choice, as well as the same form of the NJL coupling, with the same approximation, allows a comparison between our results and those of Ref. [9], see the discussion below.

![Graph](image1)

**FIG. 1:** Free energy difference $\Omega_{LOFF} - \Omega_{norm}$ in units of $10^6$ MeV$^4$ plotted versus $M_s^2/\mu$ (in MeV). The result is obtained for $\mu = 500$ MeV and $\Delta_0 = 25$ MeV. The line corresponds to the structures 1 and 2 with $\Delta_1 = 0, \Delta_2 = \Delta_3$.

In Fig. 2 we give the gaps $\Delta_I/\Delta_0$ as functions of $M_s^2/\mu$ (in MeV). The line represents the solution $\Delta_2 = \Delta_3$ for the structures 1 and 2 (in this case $\Delta_1 = 0$).

![Graph](image2)

**FIG. 2:** Gaps $\Delta_I/\Delta_0$ as functions of $M_s^2/\mu$ (in MeV) for the structures 1 and 2; the curve represents $\Delta_1 = \Delta_2 = \Delta_3$ whereas $\Delta_1 = 0$.

In Fig. 3 we present results for the electron chemical potential $\mu_e$. The line correspond to the energetically favored...
solution (structure $1 \equiv 2$; we have neglected terms suppressed in the $1/\mu$ expansion, consistently with the HDET scheme). A glance at eq. (16) shows that $\mu_e$ is given by $\mu_e \approx M_s^2/(4\mu)$, which corresponds to a symmetric splitting of the $s$ and $d$ Fermi surfaces around the $u$ Fermi surface. Therefore in this kinematical region we have $us$ and $du$ pairings, with

$$p_u + p_s = 2q_2, \quad p_u + p_d = 2q_3 = 2q_2.$$ 

The gaps $\Delta_2$ ($us$ pairing) and $\Delta_3$ ($ud$ pairing) have to be almost equal since they depend only on the absolute values of the splittings, see Fig. 2. Since the separation between the $d$ and $s$ Fermi surfaces is higher, one does not expect $ds$ pairing, which is confirmed by the result $\Delta_1 = 0$ in the region where LOFF prevails.

![Graph](image)

**FIG. 3**: The electron chemical potential $\mu_e$ as a function of $M_s^2/\mu$. Units are MeV. The line corresponds to $\Delta_2 = \Delta_3$, $\Delta_1 = 0$.

In Fig. 4 we present comparison of different phases of QCD. In order to comment this figure, let us start assuming that all the other phases are stable, meaning that in some way it is possible to cure the instability due to the imaginary gluon masses. In this case, following the graph for decreasing values of $M_s^2/\mu$, we see that at about $M_s^2/\mu = 150$ MeV the LOFF phase has a free energy lower than the normal one. This is a second order transition as it can be seen from Fig. 2. Then the LOFF state is energetically favored till the point where it meets the gCFL line at about $M_s^2/\mu = 128$ MeV. This is a first order transition since all the gaps are different in the two phases (for the gCFL case, see [8]). Then the system stays in the gCFL phase up to $M_s^2/\mu \approx 48$ MeV where it turns into the CFL phase via a second order transition (see [8]).

However, if the gapless phases are unstable, then they should not be considered, and the LOFF phase is the stable phase from $M_s^2/\mu = 150$ MeV down to about $M_s^2/\mu = 90$ MeV where the LOFF line meets the CFL line, with a first order transition (this can be seen by comparing our gaps with the $\Delta_{CFL} \approx 23$ MeV at this value of $M_s^2/\mu$).

We should also add that at the moment it is still unknown if the LOFF phase with three flavors suffers of chromo-magnetic instabilities. This problem is left to future investigations.

### VI. CONCLUSION AND OUTLOOK

We have explored in the framework of the Ginzburg-Landau expansion the LOFF phase of QCD with three flavors, using the NJL four-fermion coupling to mimic the gluon interactions. We have worked on the ansatz of a single plane wave behaviour for each quark pairing, which is the simplest generalization of the gCFL phase that takes into account the possibility of anisotropic condensation. We found that near the point where the CFL phase should give way to the normal phase, Cooper condensation takes place in the form of the LOFF pairing. Our analysis has some limitations. First, we have assumed vanishing color chemical potentials $\mu_3, \mu_8$. The results of Ref. [9] show that in the region where the LOFF state dominates the color chemical potential have rather small values, in particular smaller than $\mu_e$. However non vanishing values of $\mu_3$ and $\mu_8$ are expected to increase the LOFF free energy and therefore a more complete calculation is necessary. Second, we have considered the three possible momenta $\mathbf{q}_I$ along the same direction. Third, more than one plane wave might be present in each condensate. Finally we have treated
FIG. 4: Free energy differences $\Omega_{\text{LOFF}} - \Omega_{\text{norm}}$ in units of $10^6$ MeV$^4$ plotted versus $M_s^2/\mu$ (in MeV) for various QCD phases.

the strange quark mass at its leading effect, i.e. by a shift in its chemical potential, which is also an approximation [22]. We plan to address all these issues by a more refined study in the future.

Acknowledgments.

We wish to thank M. Mannarelli for useful discussions and comments and K. Rajagopal and R. Sharma for helpful correspondence.

[1] J. C. Collins and M.-J. Perry, Phys. Rev. Lett. 34 (1975) 1353; B. Barrois, Nucl. Phys. B129 (1977) 390; S. Frautschi, Proceedings of workshop on hadronic matter at extreme density, Erice 1978; D. Bailin and A. Love, Phys. Rept. 107 (1984) 325.

[2] M. Alford, K. Rajagopal and F. Wilczek, Phys. Lett. B422 (1998) 247, [arXiv:hep-ph/9711395].

[3] R. Rapp, T. Schäfer, E. V. Shuryak and M. Velkovsky, Phys. Rev. Lett. 81 (1998) 53, [arXiv:hep-ph/9711396].

[4] K. Rajagopal and F. Wilczek, in Handbook of QCD, M. Shifman ed. (World Scientific 2001); [arXiv:hep-ph/0011333];

[5] M. G. Alford, Ann. Rev. Nucl. Part. Sci. 51 (2001) 131, [arXiv:hep-ph/0102047]; T. Schafer, [arXiv:hep-ph/0304281]

[6] G. Nardulli, Riv. Nuovo Cim. 25N3 (2002) 1, [arXiv:hep-ph/0202007].

[7] M. Alford, K. Rajagopal and F. Wilczek, Nucl. Phys. B537 (1999) 443, [arXiv:hep-ph/9804403].

[8] I. Shovkovy and M. Huang, Phys. Lett. B 564 (2003) 205, [arXiv:hep-ph/0302142].

[9] M. Alford, C. Kouvaris and K. Rajagopal, Phys. Rev. Lett. 92, 222001 (2004) [arXiv:hep-ph/0311286].

[10] M. Alford, C. Kouvaris and K. Rajagopal, Phys. Rev. D 71 (2005) 054009 [arXiv:hep-ph/0406137].

[11] M. Huang and I. A. Shovkovy, Phys. Rev. D 70 (2004) 094030 [arXiv:hep-ph/0408268].

[12] M. Alford and Q. h. Wang, J. Phys. G 31 (2005) 719 [arXiv:hep-ph/0501078].

[13] A. I. Larkin and Yu. N. Ovchinnikov, Zh. Eksp. Teor. Fiz. 47 (1136) 1964 (Sov. Phys. JETP 20 (1965) 762); P. Fulde and R. A. Ferrell, Phys. Rev. 135 (1964) A550.

[14] M. Alford, J. A. Bowers and K. Rajagopal, Phys. Rev. D 63, 074016 (2001) [arXiv:hep-ph/0008208].
[16] J. A. Bowers and K. Rajagopal, Phys. Rev. D 66, 065002 (2002) [arXiv:hep-ph/0204079].
[17] R. Casalbuoni and G. Nardulli, Rev. Mod. Phys. 76 (2004) 263 [arXiv:hep-ph/0305069].
[18] I. Giannakis and H. C. Ren, Phys. Lett. B 611 (2005) 137 [arXiv:hep-ph/0412015].
[19] I. Giannakis and H. C. Ren, arXiv:hep-th/0504053.
[20] D. K. Hong, Phys. Lett. B 473 (2000) 118 [arXiv:hep-ph/9812510]; D. K. Hong, Nucl. Phys. B 582 (2000) 451 [arXiv:hep-ph/9905523].
[21] S. R. Beane, P. F. Bedaque and M. J. Savage, Phys. Lett. B 483 (2000) 131 [arXiv:hep-ph/0002209].
[22] R. Casalbuoni, R. Gatto, G. Nardulli and M. Ruggieri, Phys. Rev. D 68 (2003) 034024 [arXiv:hep-ph/0302077].