PERFORMANCE ASSESSMENT OF PHOSPHORIC ACID FUEL CELL - THERMOELECTRIC GENERATOR HYBRID SYSTEM WITH ECONOMIC ASPECT

Fatma Gül Çelik¹, Emin Açikkalp¹*, Hasan Yamik¹

ABSTRACT
Purpose of this paper is to evaluate phosphoric acid fuel cell (PAFC) - thermoelectric generator hybrid system with economic and thermoeconomic point of view. Firstly, basic equations of PAFC, thermoelectric generator and hybrid system are described. Secondly, basic performance parameters like power output, energy efficiency, exergy efficiency and exergy destruction rates are investigated. Finally, cost equations are set up to determine economic results of the considered system, in addition to that, these system are considered by using EXCEM analysis. According to results, the maximum total cost of the hybrid system is obtained \( j = 10900 \) am\(^{-2}\), exergy loss ratio to capital cost \( (ec) \) of the hybrid system increases dramatically after the point where \( j = 11000 \) am\(^{-2}\). Maximum power density, maximum energy efficiency and of the hybrid system are 8735.340 wm\(^{-2}\), 81.35% and 86.6% respectively.

Keywords: Phosphoric Acid Fuel Cell, Thermoelectric Generator, Hybrid System, Economic Evaluation, EXCEM Analysis.

INTRODUCTION
Fuel cell technology is the conspicuous technology because of their nearly harmless to environment, relatively higher efficiency and their flexible fuel option. Nowadays, one of the most important problem of engineers and scientists are design to systems that convert to energy as most efficiently that enable us environmental friendly usage of them. Efficiency of a heat engine are restricted by the Carnot efficiency, however, this limitations is not valid for fuel cells. Because, fuel cell generates electricity in fuel cell by electrochemical reaction. Irreversible fuel cells including Solid oxide fuel cells (SOFC), molten carbonate fuel cell (MOFC), proton exchange membrane (PEM) fuel cell, phosphoric acid fuel cell (PAFC) and direct carbon fuel cell (DCFC) are investigated [1-5]. Zhang et al. considered PAFC in [5], they investigated cell voltage for different parameters including temperature, resistances, power and efficiency of the fuel cell according to current density, load resistance and mole fraction. They defined the optimum operating conditions.

Another opportunity offered by fuel cells are that heat rejected by the fuel cell can be used in another process and fuel cell - heat engine/refrigeration hybrid systems may be designed. In last decade, irreversible fuel cell and hybrid systems have been gained attention. In ref. [6], a hybrid PAFC- absorption refrigerator system was investigated. Power densities, efficiencies are studied under different conditions like temperature, pressure and phosphoric acid mole fraction. General performance characteristics and optimum criteria of the hybrid system are shown. PAFC-heat driven refrigerator cycle was taken into account in ref. [7]. System was researched for power density and efficiency and variable parameters were defined according to current density and refrigeration temperature, finally optimum conditions and performance characteristics were obtained. Performance of different fuel cell hybrid systems can be found literature; in refs. [8-10] fuel cell-Stirling, in refs. [11-15] fuel cell – heat engine, in refs. [16-25] fuel cell- Brayton, in refs. [26,27] fuel cell-Braysson hybrid systems were investigated for different conditions and performance criteria. In addition, novel hybrid systems including fuel cell- thermionic generator and fuel cell – Super critical CO\(_2\) – Organic Rankine cycle can be seen in refs. [28, 29].

Thermoelectric generators may be an alternative for creating hybrid system with fuel cells. They have several advantageous like; they don't have moving part, noiseless and they are not required maintenance.

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¹Department of Mechanical Engineering, Engineering Faculty, Bilecik S.E. University, Bilecik, Turkey
E-mails: eacikkalp@gmail.com, emin.acikkalp@bilecik.edu.tr
Orcid id: 0000-0002-5523-7895, 0000-0001-5356-1467, 0000-0002-6269-8606
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frequently. A thermoelectric generator is used heat to generate electricity based on the Seebeck effect and similarly they can be utilized as cooler on the principle of the Peltier effect. Some authors have been researched about optimization of thermoelectric devices [28-45]. In the open literature, one can find papers about fuel cell-thermoelectric generators hybrid systems. Chen et al. analyzed PAFC-thermoelectric hybrid system for the maximum power output conditions [46]. Zhao et. al. investigated direct carbon fuel cell-thermoelectric generator hybrid system [47]. Chen et al. analyzed a PEM- thermoelectric hybrid system in terms of power output and efficiency [48]. Another alternative to evaluate and design thermal cycles is finite time thermodynamics and constructional optimization. Some example of these may be found in [49-53] and these methods can be applied for the fuel cell hybrid systems widely.

In the open literature, authors are no aware of any study about PAFC- thermoelectric hybrid system in terms of economical and thermoeconomic aspects. Such techniques seek to determine of the appropriate allocation of economic resources so as to optimize the design and/or operation of a system; and/or the economic feasibility and profitability of a system [54]. In this paper, this shortage is tried to be completed. Firstly, thermodynamic relations are expressed for the fuel cell and thermoelectric generator. Secondly, PAFC-thermoelectric generator hybrid system is analyzed with regard to power output, energy efficiency, exergy efficiency and exergy destruction rate. After these, cost of the hybrid system and thermoeconomic analysis are performed. EXCEM method [54] is chosen for the thermoeconomic evaluation. Results are obtained numerically, some important outcomes are discussed and suggestions are made.

**THERMODYNAMIC ANALYSIS**

PAFC is made of phosphoric acid as electrolyte and two electrodes which are anode and cathode. Air is provided to cathode and hydrogen is provided to anode and electrochemical reaction occurred in the fuel cell is $\text{H}_2 + \frac{1}{2} \text{O}_2 \rightarrow \text{H}_2\text{O} + \text{heat} + \text{electricity}$. This produced heat resulted from the electrochemical reaction that can be used in another process. Operating temperature of PACF is about 150-200 °C which can be used in cogeneration applications for buildings and low temperature processes. Schematic of the hybrid system is shown in fig.1. In this paper, PAFC - thermoelectric hybrid system is analyzed in terms of economical aspect. Firstly, equations for fuel cell are presented. Maximum theoretical potential or Nernst equation is [5]:

$$U_{rev} = -\frac{\Delta g^o}{n_e F} + \frac{RT}{n_e F} \ln \left( \frac{P_{H_2} \left( P_{O_2} \right)^{0.5}}{P_{H_2O}} \right)$$  \(1\)

Overpotentials cause the irreversible losses. These are activation overpotential described as activation overpotential, concentration overpotential and ohmic overpotential are shown in eqs. (2-4) respectively [5].

$$U_{act} = \frac{RT}{\alpha n_e F} \ln \left( \frac{j}{j_o} \right)$$  \(2\)

$$U_{con} = m e^{(nu)}$$  \(3\)

$$U_{ohm} = j \frac{t_{dc}}{\kappa}$$  \(4\)

where $j$ is operating current density, $j_o$ is exchange current density, $R$ is the universal gas constant, $\alpha$ is the charge transfer coefficient, $n_e$ number of electrons and $F$ is the Faraday’s constant, $T$ is the operating temperature of the fuel cell, $m$ and $n$ are two constant, $t_{dc}$ is the thickness of the electrode and $\kappa$ is the conductivity of phosphoric acid solution. The Output voltage of the PAFC is expressed as [5]:

$$U_f = U_{rev} - U_{act} - U_{con} - U_{ohm}$$  \(5\)

$$30$$
Power output and efficiency of the PAFC are calculated as eqs. (6,7) [5]:

\[ P_f = U_f jA \]  \hspace{1cm} (6)

\[ \eta_f = \frac{P_f}{-\Delta H} \]  \hspace{1cm} (7)

where \( A \) is the polar plate area, \(-\Delta H\) is the total energy provided to fuel cell per unit time and \( \Delta h \) is the molar enthalpy change at the operating temperature. \(-\Delta H\) is described in eq. (8) [5]:

\[ -\Delta H = -\frac{jA\Delta h}{n_e F} \]  \hspace{1cm} (8)

Exergy efficiency of the PAFC is:

\[ \phi_f = \frac{P_f}{-\Delta \dot{G}} \]  \hspace{1cm} (9)

where \(-\Delta \dot{G}\) Gibbs energy change per unit time and \( \Delta g \) is the molar Gibbs energy change. \(-\Delta \dot{G}\) is defined as [1]:

\[ -\Delta \dot{G} = -\frac{jA\Delta g}{n_e F} \]  \hspace{1cm} (10)
Exergy destruction rate of the fuel cell is [3]:

\[
Ex_{d,f} = \left( -\frac{\Delta h}{n_F a} - U_{cell} \right) jA
\]  

(11)

Heat transfer occurred in the regenerator is [6]:

\[
\dot{Q}_r = \theta (1 - \varepsilon_r) (T - T_o)
\]  

(12)

where \( \theta \) heat conductance, \( \varepsilon_r \), regenerator effectiveness and \( T_o \) is the ambient temperature. Heat released from the fuel cell is:

\[
\dot{Q}_{H,f} = -\Delta H - P_f - \dot{Q}_r
\]  

(13)

Secondly analysis of the thermoelectric generator must be performed. Heat input of thermoelectric generator can be defined in eqs. (14) and (16) [36]. These are equal as well as heat rejected from the PAFC in eq. (13). Heat rejected form the thermoelectric generator is shown in eqs. (15) and (17) [36].

\[
\dot{Q}_{H,j} = N \left( \beta I T_1 - I^2 \frac{r}{2} + K (T_1 - T_2) \right)
\]  

(14)

\[
\dot{Q}_{L,j} = N \left( \beta I T_2 + I^2 \frac{r}{2} + K (T_1 - T_2) \right)
\]  

(15)

\[
\dot{Q}_{H,j} = k_H a_t (T - T_1)
\]  

(16)

\[
\dot{Q}_{L,j} = k_L a_t (T_2 - T_o)
\]  

(17)

Power supplied from the thermoelectric generator is:

\[
P_t = \dot{Q}_{H,j} - \dot{Q}_{L,j}
\]  

(18)

where \( \beta \) is Seebeck coefficient, \( T_1 \) is the temperature of the hot junction, \( T_2 \) is the temperature of the cold junction, \( N \) is the number of thermoelectric units, \( I \) is the electrical current generating in semi-conductor couple, \( r \) is the electrical resistance, \( K \) is the thermal conductance of the semi-conductance couple, \( k_H \) and \( k_L \) are the heat transfer coefficients and \( a_t \) is the heat transfer area of the heat exchangers. In this study, calculations are conducted for maximum power output of the thermoelectric generator. Optimum electrical current for maximum power can be defined as [36]:

\[
I = \frac{\beta (T_1 - T_2)}{2r}
\]  

(19)

Number of modules required to heat input can be calculated by equalizing eqs. (14) and (16):
\[
N = \frac{8a_k r r (T - T_i)}{(T_i - T_r) \left(8Kr + \beta^2 (3T_1 + T_2)\right)}
\]  
(20)

Similarly, \(T_2\) is solved by equalizing eqs. (15) and (17) and result is:

\[
T_2 = \frac{3\beta^2 k_n T - 8Kk_r r - 3\beta^2 k_n T - 3\beta^2 k_i T + \beta^2 k_i T}{2a^2 k_L}
+ \sqrt{\frac{8Kk_r r + \beta^2 (3k_n T - 3k_n T + 3k_i T - 3k_i T)}{2\beta^2 k_L}}
+ 4\beta^2 k_i \left(8Kk_r (k_n T - k_i T) + k_i T + \beta^2 T_i (k_n (T - T_i) + k_i T)\right)
\]  
(21)

Finally, \(T_1\) is defined as using (13) and (16):

\[
T_1 = \left\{ \begin{array}{c}
A \Delta h_j - \frac{\Delta h_j}{F_n} - a_k n T - (1 - \varepsilon) k_n (T - T_r) - \frac{RT \ln \left( \frac{f}{j_i} \right)}{\kappa} + RT \ln \left( \frac{P_n}{P_n} \right) \\
a_k n \end{array} \right.
\]  
(22)

Thermoelectric properties depending on temperature are shown in (23) - (28) [35]:

\[
\beta = 2 \times (22224 + 930.6T_m - 0.9905T_m^2) \times 10^{-9}
\]  
(23)

\[
\rho = (5112 + 163.4T_m - 0.6279T_m^2) \times 10^{-10}
\]  
(24)

\[
\lambda = (62605 - 277.7T_m + 0.413T_m^2) \times 10^{-4}
\]  
(25)

\[
T_m = \left( \frac{T_1 + T_2}{2} \right)
\]  
(26)

\[
r = \left( \frac{\rho L_1 \rho L_2}{A_1 + A_2} \right)
\]  
(27)

\[
K = \left( \frac{\lambda A_1 + \lambda A_2}{L_1 + L_2} \right)
\]  
(28)
where $T_m$ is the mean temperature, $L_1$ is the length of p type material, $L_2$ is the length of n type material and, similarly, $A_1$ is the area of p type material, $A_2$ is the length of n type material. Efficiency and reversible power of the thermoelectric generator are shown in eqs. (29) and (30) respectively.

$$\eta_r = \frac{P_r}{\dot{Q}_{H,T}}$$  \hspace{1cm} (29)

$$P_{rev,T} = \dot{Q}_{H,T} \left(1 - \frac{T_o}{T}\right) - \dot{Q}_{L,T} \left(1 - \frac{T_o}{T_L}\right)$$  \hspace{1cm} (30)

Exergy efficiency and exergy destruction rate are expressed in eqs. (31) and (32) respectively.

$$\varphi_r = \frac{P_r}{P_{rev,T}}$$  \hspace{1cm} (31)

$$Exd_r = T_o \left(\frac{\dot{Q}_{L,T}}{T_L} - \frac{\dot{Q}_{H,T}}{T}\right)$$  \hspace{1cm} (32)

Finally, thermodynamic parameters for PAFC- thermoelectric generator is shown in (33) - (36). These are power output, efficiency, exergy efficiency and exergy destruction rate respectively.

$$P_{hy} = P_f + P_r$$  \hspace{1cm} (33)

$$\eta_{hy} = \frac{P_{hy}}{-\Delta H}$$  \hspace{1cm} (34)

$$\varphi_r = \frac{P_{hy}}{-\Delta G + P_{rev,T}}$$  \hspace{1cm} (35)

$$Exd_{hy} = Exd_f + Exd_r$$  \hspace{1cm} (36)

Firstly, hybrid system is investigated by using thermoeconomic method called EXCEM [54] where $EC$ is ratio of thermodynamic loss rate (in this paper exergy loss rate, which is described as is ratio of rate, which is difference of exergy output from the exergy input, is considered) to capital cost [54].

$$EC_k = \frac{(Exergy\ loss\ rate)_k}{Z_k}$$  \hspace{1cm} (37)

Where $Z$ is the capital cost of the system and it is calculated by multiplying unit cost ($c$) for per kW and power output of the considered system:

$$Z_k = P_k c_k$$  \hspace{1cm} (38)
Another economic evaluation criteria is the total cost of the system and it is defined as [55]:

\[
\hat{C}_k = \hat{Z}_k + \hat{C}_{\text{fuel}}
\]  

(39)

where \(\hat{Z}_k\) is capital cost to per unit of time [55]:

\[
\hat{Z}_k = \frac{Z_k \text{CRF} \Phi}{N}
\]

(40)

where \(\text{CRF}\) is the capital recovery factor, \(\Phi\) is the maintenance factor and \(N\) is the operating hours in a year [55].

\[
\text{CRF} = \frac{\ln(1+in)^{lt}}{(1+in)^{lt} - 1}
\]

(41)

In eq. (41), \(in\) represents interest rate and \(lt\) is the life time of the considered system. Fuel cost to per unit time is shown eq. (42), where \(c_{\text{fuel}}\) is unit cost of fuel, \(LHV\) lower heating value of the fuel and \(m_{\text{fuel}}\) is mass flow rate of the fuel [55]:

\[
\hat{C}_{\text{fuel}} = c_{\text{fuel}} \left(\frac{LHV}{1000}\right) m_{\text{fuel}}
\]

(42)

mass flow rate is calculated as eq (43):

\[
m_{\text{fuel}} = \left(1.05 \times 10^{-8}\right) \frac{P_j}{U_j}
\]

(43)

In calculations, parameters in eqs.(38)-(43), specific cost of the PAFC \((c_f)\) is 4$/W[56,57], specific cost of thermoelectric generator \((c_t)\) is 11.92 $/W [58], interest rate is 10%, operating house in a year is 8200 hour [55], \(\Phi\) is 1.06 [55], specific cost of the fuel \((c_{\text{fuel}})\) is 10 $/GJ [59], lower heating value of the fuel is 120.7 MJ/kg.

RESULTS AND DISCUSSION

Results obtained from calculations are shown in figs. 2-10. Parameters used in the calculations are listed in table 1 and 2 which is given from the refs. [5-7, 35-37]. Results are presented as power density \((p = P/A)\) and exergy destruction density \((\text{exd}= \text{Exd}/A)\) for power output and exergy rate.

One can be seen the change of power densities with current density in fig 2. As it is shown, all power outputs have an optimum (maximum) point. Power density of hybrid system reaches its maximum at \(j = 10200\) Am\(^{-2}\) and it is equal to 8735.340 Wm\(^{-2}\). When investigating power densities for PAFC and thermoelectric generator, it is seen that they have optimum points too. These points are provided at \(j = 10100\) Am\(^{-2}\) with 8538.440 Wm\(^{-2}\) for PAFC and at \(j = 12500\) Am\(^{-2}\) with 351.036 Wm\(^{-2}\) value for TEG. Changes of hybrid system and PAFC are parabolic, however, TEG increases nearly linear about \(j=8500\) Am\(^{-2}\) after this point it changes logarithmically and reaches its optimum.
Table 1. Parameters used in PAFC [5-7, 37].

| Parameter   | Unit     | Value   |
|-------------|----------|---------|
| $P_{H_2}, P_{H_2O}$ | atm      | 1.0347  |
| $P_{O_2}$   | atm      | 0.21    |
| $n_e$       | -        | 2       |
| $a$         | -        | 1       |
| $I_0$       | $Am^2$   | $6x10^{-2}$ |
| $t_{ele}$   | m        | $1x10^{-6}$ |
| $\kappa$    | mhom$^{-1}$ | 3.63    |
| $m$         | -        | $3x10^{-5}$ |
| $n$         | -        | $8x10^{-4}$ |
| $F$         | $C/mol$  | 96485   |
| $R$         | $J/molK$ | 8.314   |
| $\Delta g$  | $J/mol$  | $-228610$ |
| $\Delta h$  | $J/mol$  | $-243342$ |
| $T$         | K        | 473.15  |
| $epr$       | -        | 0.85    |
| $T_o$       | K        | 293.15  |

Table 2. Parameters used in thermoelectric generator [35, 36].

| Parameter | Unit      | Value |
|-----------|-----------|-------|
| $k_{H,L}$ | Wm$^{-2}$ | 170   |
| $a_t$     | m$^2$     | 1     |
| $L_1,L_2$ | mm        | 6     |
| $A_1,A_2$ | m$^2$     | 0.0001|

In figure 3 energy efficiencies are illustrated. As it is seen that they have no optimum point, their maximum values are obtained at minimum current density. Maximum efficiencies of hybrid system, PAFC and TEG are 81.35%, 81.28% and 5.51% respectively. Effect of TEG on the hybrid system increases at higher current densities, however, average effect of it on the hybrid system is about 2%.

Variation of exergy efficiencies are in fig. 4. Curves in the fig 4. is very similar in fig.3. Maximum exergy efficiencies are obtained at minimum current density and the bigger current density means the lower exergy efficiency. Maximum exergy efficiency of hybrid system is 86.6%, 86.5% for the PAFC and 14.9% for the TEG. Comparing results of energy and exergy efficiencies, it can be seen that exergy efficiencies bigger than energy efficiencies. However, effect of the TEG on the hybrid system in terms of the exergy efficiency is same with effect of the energy efficiency.

Exergy destruction densities changes are shown in fig.5. All exergy densities grow up with current density and this change nearly linear until $j = 10000 Am^{-2}$, after this point they increase dramatically. Their maximums, which are at $j = 12900 Am^{-2}$, 21473 Wm$^{-2}$ for the hybrid system, 15925 Wm$^{-2}$ for the PAFC and 5548 Wm$^{-2}$ for the TEG.

Total cost rate of the hybrid system, PAFC and TEG are indicated in fig. 6. Total cost rates of hybrid system and PAFC have an critical (maximum point) contrast to TEG. Total cost of hybrid system and PAFC increase until their critical point and then they begin to decrease. Their critical point are obtained at $j = 10900$.
Figure 2. Variation of power density with current density.

Figure 3. Variation of energy efficiency with current density.

Am$^{-2}$ for the hybrid system and $j = 10800$ Am$^{-2}$ for the PAFC and corresponding values are 0.633 Sh$^{-1}$ and 0.606 Sh$^{-1}$ respectively. The maximum total cost value of TEG is obtained at $j = 12900$ Am$^{-2}$ with 0.389 Sh$^{-1}$.
Figure 4. Variation of exergy efficiency with current density.

Figure 5. Variation of exergy destruction rate with current density.

EC of the considered systems can be shown in fig. 7. EC of all considered systems show similar tendency. EC of hybrid system and the TEG rise up nearly linear about \( j = 11000 \text{ Am}^{-2} \) and this change is very slow, after this point they increase importantly. Similarly EC of PAFC increases nearly linear until \( j = 12000 \text{ Am}^{-2} \) after this point, it grows up dramatically. Maximum values of hybrid system, PAFC and TEG are 2.782 W m\(^{-2}\), 10.922 W m\(^{-2}\), 2.491 W m\(^{-2}\) respectively and change in them are 98.6%, 99.6% and 64.9% respectively.
Figure 6. Variation of cost rate with current density.

Figure 7. Variation of EC with current density.

$p$-$\eta$-$\phi$ curves is shown in fig. 8. This chart may be called as performance curve. In this graphic, energy and exergy efficiencies of hybrid system are investigated according to power density. In there, $p_{\text{max}}, p_p, p_\phi, \eta_{\text{max}}, \eta_p, \phi_{\text{max}}, \phi_p$ mean maximum power density, power density at the maximum energy efficiency, power density at maximum exergy efficiency, maximum energy efficiency, energy efficiency at maximum power density, maximum exergy efficiency and exergy efficiency at the maximum power density. $\eta_p$ and $\phi_p$ are equal to 67.9%.
and 72.3%, these values correspond to 82.7% and 83.4% of their maximum respectively. $p_{\eta}$ and $p_{\phi}$ are equal to each other and their values are 205.173 Wm\(^{-2}\) and it is equal to only 2.3% of the maximum power density.

$p$-$C$-$EC$ curves can be shown in fig.9 where $p_{C}$, $p_{EC}$, $C_{max}$, $C_{p}$, $EC_{max}$, $EC_{p}$ represent to power density at total cost rate, power density at EC, maximum total cost rate, total cost rate at power density, maximum exergy loss rate and EC at maximum power density respectively. $p_{C}$ is equal to 8485.99 Wm\(^{-2}\) which is 97.1% of the maximum power density and $p_{EC}$ is 8397.20 Wm\(^{-2}\) which is equal to 96.1% of the maximum power density.

Figure 8. $p$-$\eta$-$\phi$ curve for the hybrid system.

Figure 9. $p$-$C$-$EC$ curve for the hybrid system.
Similarly, $\dot{C}_p$ is 0.620 and it is 98% of the maximum total capital cost rate and $EC_p$ is equal to 0.0917 W$^{-1}$ which is only 3.3% of the maximum $EC$.

Finally, $\eta$--$\dot{C}$-$EC$ chart is indicated in fig.10 where $\eta_C$, $\eta_{EC}$. $\dot{C}_{max}$, $\dot{C}_\eta$, $EC_{max}$ $EC_\eta$ are energy efficiency at the maximum total capital cost rate, energy efficiency at the maximum $EC$, maximum total capital cost rate, total capital cost rate at the maximum energy efficiency, maximum $EC$ and $EC$ the maximum energy efficiency respectively. $\eta_C$ and $\eta_{EC}$ are 61.7% and 4.1%, these values correspond to 75.8% and 5% of the maximum efficiency. In addition to that $\dot{C}_\eta$ and $EC_\eta$ are 0.013 Sh$^{-1}$ and 0.039 W$^{-1}$, these values are 2% and 1.4% of their maximum.

CONCLUDING REMARKS

In this paper, a PAFC-TEG hybrid system is investigated in terms of its performance, economical and thermoeconomic aspects. Some important results are listed follows:

- Maximum power density of the hybrid system is 8735.340 Wm$^{-2}$ at $j= 10200$ Am$^{-2}$.
- Maximum energy efficiency of the hybrid system is 81.35% at low current densities, effect of TEG on the hybrid system 2% on average. Maximum exergy efficiency of the hybrid system is 86.6%, and it is obtained at low current densities similar to energy efficiency.
- The maximum total cost of the hybrid system is obtained $j= 10900$ Am$^{-2}$ and this cost is equal to 0.633 Sh$^{-1}$
- The maximum $EC$ of hybrid system is 10.922 W$^{-1}$.
- Exergy loss rate of the hybrid system increases dramatically at $j= 11000$ Am$^{-2}$ and it is equal to 15925 Wm$^{-2}$.

As it is shown where the maximum power density, the total cost rate is maximum too, until 11000 Am$^{-2}$ exergy lost rate does not change so importantly. In addition to these, energy efficiency, exergy efficiency and exergy destruction rate are high and the total cost rate, exergy loss rate have low values at the small current densities. According to these results, current densities should be chosen as low as possible in terms of economic aspects, economical and thermoeconomic analyses are recommended to be conducted for fuel cell hybrid systems.
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NOMENCLATURE

$A$  polar rate area [m$^2$]
$a$  heat transfer area [m$^2$]
$c$  unit cost for per kW [SkW$^{-1}$]
$\dot{C}$  heat capacity [Sh$^{-1}$]
$CRF$  Capital recovery factor
$EC$  ratio of thermodynamic loss rate to capital cost [kW$/h$]
$exd$  exergy destruction density [Wm$^{-2}$]
$Exd$  exergy destruction rate [W]
$F$  Faraday constant [Cmol$^{-1}$]
$\Delta g$  change of the molar Gibbs free energy [Jmol$^{-1}$]
$\Delta \dot{G}$  change rate of the molar Gibbs free energy [W]
$\Delta h$  change of the molar enthalpy [Jmol$^{-1}$]
$\Delta \dot{H}$  change rate of the enthalpy [W]
$I$  electrical current generating in semi-conductance couple [A]
$j$  current density [Am$^{-2}$]
$k$  heat transfer coefficient [W m$^{-2}$ K$^{-1}$]
$K$  heat conductance of the semi-conductance couple [W m$^{-1}$ K$^{-1}$]
$L$  length of p and n type material [mm]
$LHV$  lower heating value of the fuel [kJ kg$^{-1}$]
$m$  a constant
$\dot{m}$  mass flow rate [kgs$^{-1}$]
$n$  number electrons and a constant
$N$  number of thermoelectric units and operation hours in a year [hyear$^{-1}$]
$P$  pressure [atm, kPa], power density [Wm$^{-2}$]
$P_{AFC}$  phosphoric acid fuel cell
$\dot{Q}$  heat rate [W]
$r$  electrical resistance of the semiconductor couple [Ω]
$R$  universal gas constant [Jmol$^{-1}$K$^{-1}$]
$t$  thickness [m]
$T$  temperature [K]
$TEG$  thermoelectric generator
$U$  potential [V]
$Z$  capital cost [$S$]
$\dot{Z}$  capital cost per hour [$Sh^{-1}$]

Subscripts

$act$  activation
$C$  heat capacity
$con$  concentration
$EC$  ratio of thermodynamic loss rate to capital cost
$f$  fuel cell
$m$  mean
$e$  electron
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