Star formation along the Hubble sequence:
Radial structure of the star formation of CALIFA galaxies

R. M. González Delgado¹, R. Cid Fernandes², E. Pérez¹, R. García-Benito¹, R. López Fernández¹, E. A. D. Lacerda¹,², C. Cortijo-Ferrero¹, A. L. de Amorim², N. Vale Asari², S. F. Sánchez¹, C. J. Walcher³, L. Wisotzki⁴, D. Mast⁵, J. Alves⁶, Y. Ascasibar⁷,⁸, J. Bland-Hawthorn⁹, L. Galbany¹⁰,¹¹, R. C. Kennicutt Jr.¹², I. Márquez¹, J. Masegosa¹, M. Mollá¹³, P. Sánchez-Blázquez⁷,⁸, J. M. Vílchez¹, CALIFA collaboration¹⁴

(Affiliations can be found after the references)

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ABSTRACT

The spatially resolved stellar population content of today’s galaxies holds important information to understand the different processes that contribute to the star formation and mass assembly histories of galaxies. The aim of this paper is to characterize the radial structure of the star formation rate (SFR) and mass in galaxies in the nearby Universe as represented by a unique rich and diverse data set drawn from the CALIFA survey. The sample under study contains 416 galaxies observed with integral field spectroscopy, covering a wide range of Hubble types and stellar masses ranging from $M_\ast \sim 10^9$ to $7 \times 10^{11} M_\odot$. Spectral synthesis techniques are applied to the datacubes to derive 2D maps and radial profiles of the intensity of the star formation rate in the recent past ($\Sigma_{SFR}$), as well as related properties such as the local specific star formation rate (sSFR), defined as the ratio between $\Sigma_{SFR}$ and the stellar mass surface density ($\mu_\ast$). To emphasize the behavior of these properties for galaxies that are on and off the main sequence of star formation (MSSF) we stack the individual radial profiles in seven bins of galaxy morphology (E, S0, Sa, Sb, Sbc, Sc, and Sd), and several stellar masses. Our main results are: (a) The intensity of the star formation rate shows declining profiles that exhibit very little differences between spirals, with values at $R = 1$ half light radius (HLR) within a factor two of $\Sigma_{SFR} \sim 2 \cdot 10^2 M_\odot yr^{-1} pc^{-2}$. The dispersion in the $\Sigma_{SFR}$ (R) profiles is significantly smaller in late type spirals (Sbc, Sc, Sd). This confirms that the MSSF is a sequence of galaxies with nearly constant $\Sigma_{SFR}$. (b) SFR values scale with Hubble type and increase radially outwards, with a steeper slope in the inner 1 HLR. This behavior suggests that galaxies are quenched inside-out, and that this process is faster in the central, bulge-dominated part than in the disks. (c) As a whole, and at all radii, E and S0 are off the MSSF, with SFR much smaller than spirals of the same mass. (d) Applying the volume-corrections for the CALIFA sample, we obtain a density of star formation in the local Universe of $\Sigma_{SFR} = 0.0105 \pm 0.0008 M_\odot yr^{-1} Mpc^{-3}$, in agreement with independent estimates. Most of the star formation is occurring in the disks of spirals. (e) The volume averaged birthrate parameter, that measures the current SFR with respect to its lifetime average, $b^\prime = 0.39 \pm 0.03$, suggests that the present day Universe is forming stars at $\sim 1/3$ of its past average rate. E, S0, and the bulge of early type spirals (Sa, Sb) contribute little to the recent SFR of the Universe, which is dominated by the disks of Sbc, Sc, and Sd spirals. (f) There is a tight relation between $\Sigma_{SFR}$ and $\mu_\ast$, defining a local MSSF relation with a logarithmic slope of 0.8, similar to the global MSSF relation between SFR and $M_\ast$. This suggests that local processes are important in determining the star formation in disks, probably through a density dependence of the SFR law. The scatter in the local MSSF is driven by morphology-related offsets, with $\Sigma_{SFR}/\mu_\ast$ increasing from early to late type galaxies, indicating that the shut down of the star formation is more related with global processes, such as the formation of a spheroidal component.

Key words. Techniques: Integral Field Spectroscopy – galaxies: evolution – galaxies: stellar content – galaxies: structure – galaxies: fundamental parameters – galaxies: bulges – galaxies: spiral

1. Introduction

Nearly a century later, the simple classification scheme introduced by Hubble [1936] is still in use. The reason it remains useful is that the physical properties of galaxies correlate with the morphology in a broad context (e.g. Holmberg 1958; Roberts & Haynes 1994). In particular, the Hubble sequence can be described as a sequence in terms of recent star formation, increasing in importance from elliptical (E) to spiral (S) galaxies (e.g. Kennicutt 1983a, 1998).

Contemporary galaxy surveys have mapped this bimodal distribution implicit in the Hubble classification in terms of properties related with their structure (morphology), stellar content, and chemical composition (e.g. Blanton et al. 2003; Baldry et al. 2004; Blanton & Moustakas 2009; Kauffmann et al. 2003; Mateus et al. 2006; Ascasibar & Sánchez Almeida 2011; Casado et al. 2015). One population, located in the region of the color-magnitude diagram (CMD) known as the red sequence, is composed of galaxies with little star formation, large stellar masses ($M_\ast$), stellar mass surface density ($\mu_\ast$), and light concentration. The other major population, located in the so-called blue cloud in the CMD, consists of galaxies with significant star formation, smaller $M_\ast$ and $\mu_\ast$, and small concentration in light. The red sequence is the realm of early type galaxies, whereas galaxies of later Hubble types populate the blue cloud.

Other works have shown that galaxies that populate the blue cloud follow a strong correlation between $M_\ast$ and the present star formation rate (SFR) (Brinchmann et al. 2004; Salim et al. 2007; Renzini & Peng 2015; Catalan-Torrecilla et al. 2015); the main-sequence of star forming galaxies (MSSF). The correlation is tight, with only 0.2–0.3 dex dispersion in SFR for a fixed $M_\ast$, and with a slope that is somewhat smaller than unity, implying that the relative rate at which stars form in galaxies, i.e. the specific star formation rate $sSFR = SFR/M_\ast$, declines weakly with...
increasing galaxy mass \cite{Salim2007, Schiminovich2007}.

Subsequent studies have shown that the MSSF relation persists to at least $z \sim 4$ \cite[e.g.][]{Noeske2007, Daddi2007, Elbaz2007, Peng2010, Wuyts2011}. These works conclude that most of the star formation in the Universe is produced by galaxies in the main sequence, with starbursts (which deviate upwards from the MSSF) contributing with only $\sim 10\%$ to the total star formation rate at $z \sim 2$ \cite[Sanders & Mirabel1996, Rodrigiero et al.2011], where the peak of the cosmic star formation rate occurs \cite[e.g.][]{Madau2014}. A recent study by \cite{Speagle2014} finds that the logarithmic slope of the MSSF relation increases with cosmic time, from $-0.6$ at $z \sim 2$ to $0.84$ at $z = 0$. This implies that the characteristic sSFR of the main sequence population evolves rapidly with redshift \cite{Karim2011}. In fact, Elbaz et al.\cite{2011} show that star formation has decreased by a factor of 20 since $z \sim 2$, and that the corresponding sSFR declined as $r^{-2}$, where $r$ is the cosmic epoch.

There is also a substantial population of quenched galaxies that dominate the high end of the mass function, but whose sSFR is significantly lower than in star forming galaxies \cite{Salim2007, Schiminovich2007, Chang2015}. In a simple picture, galaxies evolve along the blue star forming MSSF, increasing in mass through the accretion of cold gas from the cosmic web and/or mergers. When it approaches a critical mass the supply of gas is shut off. Star formation is thus quenched and the galaxy migrates to the red sequence, where the increase in mass and size may happen through minor mergers \cite[e.g.][]{Faber2007, Lilly2013}. Although the quenching phase is relevant in the life of a galaxy, it is not clear at which critical mass the galaxy is quenched, and whether this is related with a change in the nature of the gas accretion, with heating of the surrounding gas by an AGN, or with the formation of an spheroidal component \cite{Martig2009}.

Evidently, this whole field relies on empirical measures of the SFR. There is no shortage of methods to estimate the SFR, each with its virtues and caveats \cite{Kennicutt2012} for a review. Some gauge the SFR indirectly by quantifying how the radiative output of young stars is reprocessed by gas or dust, as $H\alpha$ and far infra-red SFR indicators. Direct detection of recently formed stars is best done in the UV, where they outshine the optical stellar continuum. The goals are: 1) To characterize the SFH and explain how we measure the present SFR. Section 4 describes the observations and summarizes the properties of the galaxies analyzed here. In Section 3 we summarize our method for extracting the SFH and explain how we measure the present SFR. Section 2 presents results on the MSSF relation and how our assumptions affect it. Section 5 deals with the radial structure of the inten-
sity of the star formation rate ($\Sigma_{\text{SFR}}$), and related properties such as the local specific SFR. We discuss the results and their relation with the cosmic star formation of the local Universe in Section 6. Section 7 summarizes our main findings.

2. Data and sample

2.1. Observations and data reduction

The observations were carried out with the Potsdam Multi-Aperture Spectrometer PMAS (Roth et al. 2005) in the PPaK mode (Verheijen et al. 2004) at the 3.5m telescope of Calar Alto observatory. PPaK contains 382 fibers of 2.7" diameter each, and a 74" × 64" FoV (Kelz et al. 2006). Each galaxy is observed with two spectral settings, V500 and V1200, with spectral resolutions ~ 6 (FWHM) and 2.3 Å, respectively. The V500 grating covers from 3745 to 7300 Å, while the V1200 covers 3650–4840 Å. To reduce the effects of vignetting on the data, we combine the observations in the V1200 and V500 setups, calibrated with version 1.5 of the reduction pipeline. We refer to Sánchez et al. (2012), Husemann et al. (2013), and García-Benito et al. (2015) for details on the observational strategy and data processing.

2.2. Sample: morphological classification

The CALIFA mother sample consists of 939 galaxies selected from the SDSS survey in the redshift range $z = 0.005–0.03$, and with $r$-band angular isophotal diameter of 45–80". It is primarily a diameter-limited sample to guarantee that the objects fill the 74" × 64" FoV. It includes a significant number of galaxies in different bins in the CMD, and covers a wide and representative range of galaxy types. The galaxies were morphologically classified by five members of the collaboration through visual inspection of the SDSS $r$-band images, averaging the results (after clipping outliers). The sample and its characteristics are fully described in Walcher et al. (2014).

The targets studied in this paper were selected from those observed in both V1200 and V500 setups earlier than January 2015, and excluding type 1 Seyferts and galaxies that show merger or interaction features. This leaves a final sample of 416 galaxies.

As we have done in GD15, we group the galaxies into seven morphology bins: E (57 galaxies), S0 (54, including S0 and S0a), Sa (70, including Sa and Sab), Sb (70), Sbc (76), Sc (69, including Sc and Scd), and Sd (20, including 18 Sd, 1 Sm, and 1 Irr). Fig. 1 shows the morphological distribution of our 416 galaxies (filled bars) as well as that of the mother sample (empty bars). The histograms are normalized to unity, so that the two distributions are directly comparable. The number of galaxies in each morphology bin is labeled in color, with the same palette used throughout the paper.

3. Stellar population analysis: Mass and star formation rate

3.1. Method of analysis

To extract the stellar population properties from the datacubes we apply the same method than in Pérez et al. (2013), Cid Fernandes et al. (2013, 2014), and González Delgado et al. (2014b, a, 2015). Briefly, after some basic pre-processing steps like spatial masking of foreground and background sources, rest-framing, and spectral resampling, the individual spectra that have signal-to-noise ratio $S/N \leq 20$ in a 90 Å window centered at 5635 Å (rest-frame), are coadded into Voronoi zones (Capacci & Copin 2003). The resulting 366112 spectra (880 per galaxy, on average) are then fitted with starlight (Cid Fernandes et al. 2005) using the cluster Grid-CSIC at the Instituto de Astrofísica de Andalucía. The output is then processed through pycasso (the Python CALIFA Stellar Synthesis Organizer) to produce a suite of the spatially resolved stellar population properties.

The base used in starlight’s spectral decomposition is a central ingredient in our whole analysis. The results presented here were obtained with base GMc, as defined in González Delgado et al. (2014b, a, 2015). This base comprises 235 spectra for simple stellar populations (SSP) drawn from Vazdekis et al. (2010) for populations older than $t = 63$ Myr and from González Delgado et al. (2005) models for younger ages. The evolutionary tracks are those of Girardi et al. (2000), except for the youngest ages (1 and 3 Myr), which are based on the Geneva tracks (Schaller et al. 1992; Schaerer et al. 1996; Charbonnel et al. 1993). The Initial Mass Function (IMF) is Salpeter. The Z range covers the seven metallicities provided by Vazdekis et al. (2010) models: $\log Z/Z_{\odot} = -2.3, -1.7, -1.3, -0.7, -0.4, 0$, and +0.22, but SSPs younger than 63 Myr include only the four largest metallicities. The Appendix presents some comparisons with results obtained with an alternative base built from a preliminary update of the Bruzual & Charlot (2003) models.

3.2. Stellar masses

Our galaxy stellar masses ($M_*$) are obtained by adding the masses of each spatial zone (Cid Fernandes et al. 2013, González Delgado et al. 2015). This procedure takes into account spatial variations of the stellar population properties and stellar extinction, something which cannot be done when dealing with integrated light data (i.e., one spectrum per galaxy). Masked spaxels, due to foreground stars or other artifacts, are corrected for in

![Fig. 1. Comparison of the distribution of Hubble types in the CALIFA mother sample (939 galaxies, bars) and the 416 galaxies analyzed here (filled narrow color bars). The histograms are normalized to unity, so that the two distributions are directly comparable. The number of galaxies in each morphology bin is labeled in color, with the same palette used throughout the paper.](image-url)
Table 1. Number of galaxies in each Hubble type and mass interval. 

| log $M_\star(M_{\odot})$ | E   | S0  | Sa  | Sb  | Sbc | Sc  | Sd  |
|-------------------------|-----|-----|-----|-----|-----|-----|-----|
| $\leq 9.1$               | -   | -   | -   | -   | -   | -   | 1   |
| 9.1–9.6                 | -   | -   | -   | -   | -   | 15  | 11  |
| 9.6–10.1                | 1   | 2   | -   | 5   | 14  | 5   | -   |
| 10.1–10.6               | 1   | 3   | 10  | 14  | 28  | 3   | -   |
| 10.6–10.9               | 7   | 15  | 19  | 29  | 4   | 0   | -   |
| 10.9–11.2               | 16  | 18  | 28  | 22  | 20  | 6   | -   |
| 11.2–11.5               | 19  | 15  | 20  | 14  | 4   | 1   | -   |
| 11.5–11.8               | 13  | 2   | -   | -   | -   | -   | -   |
| $\geq 11.8$             | 1   | -   | -   | -   | -   | -   | -   |
| total (416)             | 57  | 54  | 70  | 70  | 76  | 69  | 29  |

Average light (upper panel) and mass (bottom) fractions (defined with respect to $\lambda = 5635$ Å, the normalizing wavelength) due to stars in different age ranges as a function of Hubble type. Age ranges are coded by color: The youngest ones, $< 32$ Myr, in violet (hardly visible in the bottom panel because they carry little mass). Populations from 32 to 900 Myr are shown in green; those from 0.9 to 2 Gyr in orange, and older ones in red.

pycasso using the stellar mass surface density ($\mu_\star$) radial profile as explained in González Delgado et al. (2014b).

Both $M_\star$ and Hubble type play important roles in this paper, so it is important to know how these two properties relate to each other. Table 1 shows the distribution of galaxies by Hubble type in several bins of $M_\star$. The masses range from $8 \times 10^8$ to $7 \times 10^{11} M_\odot$ (for a Salpeter IMF), and peak at $\sim 10^{11} M_\odot$. As expected, $M_\star$ correlates with Hubble type (see also González Delgado et al. 2015, particularly their Fig. 2). E are the most massive galaxies with log $M_\star = 11.3 \pm 0.3$ (average $\pm$ dispersion) in solar units, and the least massive galaxies are those in the Sd bin, with log $M_\star = 9.6 \pm 0.4$. The more typical CALIFA galaxy has log $M_\star = 10.75$, similar to the Milky Way’s mass (Licquia & Newman 2015).

3.3. Estimation of the recent SFR from the spectral synthesis

SFR is usually estimated from H$\alpha$, far-infrared, or UV luminosities (Kennicutt 1998; Kennicutt & Evans 2012; Catalán-Torrecilla et al. 2015), which, despite their own caveats and limitations, get the job done with conveniently simple, one-line formulae. No such straightforward recipe exists for optical continuum data, however. The reason is that stars of all ages can make comparable contributions to the optical light, and isolating the part due to those formed in the recent past is not a trivial task. It is, however, a feasible one. After all, decomposing a spectrum in terms of stellar populations of different ages is precisely what starlight does. In fact, an extended version of the code is being developed which incorporates UV, far-infrared, and/or emission line information (López Fernández et al. 2016), all of which should improve its sensitivity to young stars. In any case, as shown by Asari et al. (2007), the standard version of starlight already performs well in this respect.

This section explains our methodology to compute SFRs. The SFR values themselves are presented in later sections, while the discussion here focuses on how to handle the starlight output to produce meaningful SFR estimates, the uncertainties involved, and how to improve the results by means of criteria based on ancillary emission line information.

3.3.1. Choice of a "recent" star formation time scale

Let us first specify what we mean by “recent past” by defining $t_{SF}$ as the age of the oldest stars to be included in the computation of our recent SFR. The mean rate of star formation then follows from a simple summation over all populations younger that $t_{SF}$:

$$SFR_{xy} = \frac{1}{t_{SF}} \sum_{t \leq t_{SF}} M_{\star xy}$$

where $xy$ denotes a spaxel (or Voronoi zone) and $M_{\star xy}$ is the mass initially turned into stars which now have age $t$ at the same $xy$ location. Radial profiles of SFR and galaxy wide rates are trivially obtained by averaging SFR$_{xy}$ over the desired $xy$ region. Similarly, surface densities ($\Sigma_{SFR}$) are obtained by dividing by the corresponding area (a spaxel, a radial ring, the whole galaxy, etc.).

The choice of $t_{SF}$ is arbitrary, so let us sketch some general guidelines to choose a useful value. Naturally, the larger $t_{SF}$ is, the more robust the corresponding SFR becomes, since more base elements are summed over in eq. (1), thus minimizing known degeneracies in stellar population synthesis (e.g., Cid Fernandes et al. 2014). On the other hand, one would like $t_{SF}$ to be much smaller than the Hubble time (otherwise SFR and $M_\star$ become equivalent quantities). Furthermore, it would be desirable to have a $t_{SF}$ of the same order of magnitude.

After some experimentation we chose $t_{SF} = 32$ Myr. This choice follows the same rationale (but different data) as in Asari et al. (2007), who, in a study of star-forming galaxies in the SDSS, found that a very similar time-scale (25 Myr; see their figure 6) produces the best correlation between starlight and 1 This overly precise looking value of $t_{xy}$ merely reflects the choice of which ages in our discrete grid to include in the summation in eq. (1). We chose to include up to the base element at $t = 32$ Myr (actually 31.62 Myr).
For the purposes of this paper it suffices to say that $t_{SF}$-values between $\sim 10$ and 100 Myr would lead to the same overall qualitative conclusions.

### 3.3.2. SFHs along the Hubble sequence: a condensed view

Fig. 2 tracks the percent contribution in light (top panels) and mass (bottom) of our recent populations ($\leq t_{SF} = 32$ Myr, in magenta) along the Hubble sequence, as well as those of stars in three other intervals: 32 Myr to 0.9 Gyr (green), 0.9 to 2 Gyr (orange), and $\geq 2$ Gyr (red). These four intervals roughly represent populations in which the light is dominated by O, B, A–early F, and later type (lower mass) stars. This strategy of grouping stellar populations in broad age-ranges as a way of summarizing SFHs goes back to early studies based on equivalent widths and colors (Bica 1988; Bica et al. 1994; Cid Fernandes et al. 2001).

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The top panels in Fig. 2 show a steady progression of young and intermediate age populations along the Hubble sequence. The percent light contribution (at $\lambda$) to a future communication (Lacerda et al., in prep.) between $\sim$ 0.9 to 2 Gyr (or-ange), and $\geq 2$ Gyr (red). These four intervals roughly represent populations in which the light is dominated by O, B, A–early F, and later type (lower mass) stars. This strategy of grouping stellar populations in broad age-ranges as a way of summarizing SFHs goes back to early studies based on equivalent widths and colors (Bica 1988; Bica et al. 1994; Cid Fernandes et al. 2001). but was also applied in full spectral fitting work (González Delgado et al. 2004; Cid Fernandes et al. 2004; 2005).

### 3.3.3. Star formation in early type galaxies

The contribution of young stars decreases even further towards E and S0, but it is not null, with $x_y \sim 2\%$. Naturally, the reality of populations accounting for so little light is questionable. Based on the extensive set of simulations carried out by Cid Fernandes et al. (2014) to evaluate uncertainties in the star formation rates for CALIFA-like data, we estimate the level of noise-induced uncertainty in $x_y$ to be of the order of $3\%$. Given this, the small $x_y$ fractions identified in E and S0 should be considered noise. However, this $3\%$ error estimate reflects the level of uncertainty expected for a single spectral fit, whereas the $x_y \sim 2\%$ in the top left of Fig. 2 reflects an average over 115927 zones inside of the central 3 kpc of E galaxies. Looking from this statistical angle one should perhaps take the small $x_y$ fractions in these systems as a sign that they may not be so quiescent after all. There is in fact evidence for some level of star formation in at least some early type galaxies (Kaviraj et al. 2007). In the context of CALIFA data, Gomes et al. (2015b) have unveiled spiral-arm-like features consistent with recent star formation in three early type galaxies.

In any case, at such low $x_y$-levels one also needs to worry about systematic effects, and the study by Ocvirk (2010) is specially relevant in this respect. He finds that blue horizontal branch stars can easily masquerade as massive young stars in spectral fits, creating the artificial impression of recent star formation in otherwise genuinely old populations. This same effect was in fact detected in previous STARLIGHT-based work on both globular clusters (Cid Fernandes & González Delgado 2010) and passive galaxies (Cid Fernandes et al. 2011), and ultimately reflects limitations in the modeling of stellar evolution embedded in the SSP models used in our spectral decomposition.

As will soon become clear, for the purposes of this paper the exact values of SFR or $\Sigma_{SFR}$ in E and S0 galaxies are not as important as the fact that their star forming properties are markedly different from those of later type galaxies, a relative behavior which is safely immune to the uncertainties discussed above.

### 3.3.4. The equivalent width of Hα as an ancillary constraint

The above raised issue of the reliability of the recent star formation derived from our optical spectral synthesis analysis is relevant to all our galaxies, not only to early type ones. We now seek for ways to filter out or at least flag objects where starlight-based SFRs are not reliable enough.

A possible first-cut solution would be to plainly eliminate all data points where $x_y$ is below, say, twice its uncertainty. Adopting the $\sigma(x_y) \sim 3\%$ typical uncertainty from the simulations of Cid Fernandes et al. (2014) would then lead to a $x_y > 6\%$ two-sigma criterion to select reliable individual galaxy zones.

We chose to define a criterion based on entirely different precepts. The idea is to use the Hα emission equivalent width ($W_{HA}$) to guide our decision on whether STARLIGHT-derived SFR is indeed tracing recent star formation reliably or not. The rationale goes as follows: (1) The recent populations we aim to trace are young enough to photoionize the surrounding gas into HII regions, and hence produce Hα. (2) Stellar evolution plus straightforward nebular physics predicts a floor-value of $W_{HA}$ in the range of 1–3 Å, corresponding to the limit where the interstellar medium is photoionized by hot, old, low mass, evolved stars (HOLMES, as defined by Flores-Fajardo et al. 2011). Systems with $W_{HA} \leq 3 \AA$ must therefore have stopped forming stars very long ago, a regime dubbed as “retired galaxy” by Stasinska et al. (2008) and Cid Fernandes et al. (2011).

This whole scheme is based on the idea that both $x_y$ and $W_{HA}$ trace recent star formation, a corollary of which is that they are correlated. This expectation is fully born out by our data, as seen in the left panel of Fig. 3. The plot shows a (log-scale) density map of $W_{HA}$ versus $x_y$ for 11894 radial points where Hα emission could be measured. White circles trace the mean $W_{HA}$ values in $x_y$ bins, and the grey line shows the corresponding linear fit. We point out that, although expected, this empirical correlation is in no sense tautological, since the two axes are derived from completely independent observable $x_y$. In fact, we regard this independence as an added benefit of our approach.

Points with $W_{HA} < 3 \AA$ in the left panel of Fig. 3 have on average $x_y = 3.4\%$. This limit on $W_{HA}$ is based both on the observed bimodal distribution of $W_{HA}$ in local Universe galaxies and on long-known theoretical expectations (Cid Fernandes et al. 2011; Sánchez et al. 2015a) to propose a more stringent $W_{HA} > 6 \AA$ cut to isolate regions ionized by young stars. The mean $x_y$ for populations with weaker $W_{HA}$ is 4.3%, very close to that obtained with the Cid Fernandes et al. (2011) criterion. Dashed and

\[2\text{ Strictly speaking $W_{HA}$ does depend on the STARLIGHT run, since the line flux is measured over the residual spectrum obtained after subtracting the STARLIGHT fit, but this is only a "second order" dependence.}\]

\[3\text{ The $W_{HA}$ values expected for galaxies where HOLMES dominate the ionizing flux is in the 0.5–2.4 Å range (Binette et al. 1994; Cid Fernandes et al. 2011; Gomes et al. 2015a). Our $W_{HA} < 3 \AA$ limit adds a (small) safety cushion to this prediction.}\]
dotted lines mark \( W_{\text{H}}(x_{Y}) = (3 \, \AA, 3.4\%) \) and \((6 \, \AA, 4.3\%)\) in Fig. 3, respectively. It is clear that adopting either of these cuts should not lead to significantly different results.

Before elaborating more on the effects of \( W_{\text{H}} \) and \( x_{Y} \) reliability criteria, let us first examine how these two properties vary across the face of galaxies.

### 3.3.5. The radial profiles of \( W_{\text{H}} \) and \( x_{Y} \)

The middle and right panels in Fig. 3 show the average radial profiles of \( W_{\text{H}} \) and \( x_{Y} \) for the seven morphological bins. Dashed and dotted lines mark the same \( (W_{\text{H}}(x_{Y}), x_{Y}) \) limits as in the left panel. As in our previous papers (e.g., González Delgado et al. 2014b), these average profiles are constructed by first expressing the radial distance for each galaxy in units of the corresponding half light radius (HLR), defined as the length of the elliptical aperture along the major axis that contains half of the total flux at 5635 Å (rest-frame) within the field of view of PPaK.

The vertical ordering of Hubble types in the middle and right panels of Fig. 3 follows the expected tendency, with late type systems being more star-forming than early type ones. Focusing on the lower part of the plots, we see that E and S0 have mean \( W_{\text{H}} < 3 \, \AA \) at all locations, confirming that the extended \( \text{H}_\alpha \) emission in these systems is consistent with being produced from photoionization by old stars (Sarzi et al. 2006; Kehrig et al. 2012; Papaderos et al. 2013; Singh et al. 2013; Gomes et al. 2015a). Whatever little star formation remains in these early type galaxies it is the exception, not the rule. Furthermore, such residual star formation would be located towards the outskirts of these galaxies, as indicated by the rise in their \( x_{Y}(R) \) profiles, reaching 3–5% for \( R \geq 2 \, \text{HLR} \).

Moving to Sa galaxies, we see that, on average, they have \( W_{\text{H}} > 3 \, \AA \) at all radii, although they get close to this limit in their central regions (probably reflecting a contribution from retired bulges). Also, except for the central 0.5 HLR, \( x_{Y}(R) \) values are all above the 3.4% line. Beyond 1 HLR their mean \( W_{\text{H}} \) oscillates around 6 Å, so a < 6 Å cut would remove significant portions of their disks. Finally, Fig. 3 shows that whichever reliability cut we chose to apply would make little difference for Sb and later type galaxies.

In what follows we shall give more emphasis to results obtained by applying a \( x_{Y} > 3.4\% \) cut when computing SFR through equation [1] but results obtained with the alternative \( W_{\text{H}} > 3 \) or 6 Å criteria will also be presented for completeness.

In the next section we explore the impact of these three different criteria on the galaxy-wide SFR and the correlation between \( M_{\star} \) and SFR.

### 4. The global main sequence of star forming galaxies

As reviewed in the introduction, the main sequence of star forming galaxies (MSSF) is the name given to the correlation between SFR and \( M_{\star} \) (Noeske et al. 2007). This correlation has been found in star forming galaxies of the local Universe (Brinchmann et al. 2004), and seen to persist at least to redshift \( z \sim 4 \) (Peng et al. 2010; Wuyts et al. 2011). The logarithmic slope of the relation varies in the range from 0.4 to 1, depending on the galaxy selection criteria and on the indicator used to estimate the SFR (Speagle et al. 2014). Recently, Renzini & Peng (2015) proposed to characterize the main sequence by the ridge line of the star forming peak in a 3D SFR-\( M_{\star} \)-Number plot obtained with the SDSS sample. Their objective definition leads to a best fit line given by log SFR \( (M_{\odot} \, \text{yr}^{-1}) = (0.76 \pm 0.01) \times \log M_{\star} (M_{\odot}) - (7.64 \pm 0.02) \).

Fig. 4 shows three versions of the log SFR vs. log \( M_{\star} \) relation obtained with our data and methods. We call this relation the “global MSSF”, in contrast to the “local MSSF” where SFR and \( M_{\star} \) values are replaced by their respective surface densities (cf. Sec. 6.3 below and Cano-Díaz et al. 2016). The total SFR is calculated for each galaxy using Eq. [1] and adding the contribution of all spaxels that verify \( x_{Y} > 3.4\% \) (panel a), \( W_{\text{H}} > 3 \)
Typical of early type galaxies. Note that the masses are the same as resulting from different selection criteria imposed on the individual spaxels included in the computation of the galaxy’s total SFR = Σ, SFRxy. Only xy > 3.4% (left), W_Hα > 3 Å (middle), and W_Hα > 6 Å (right).

The dashed gray-blue lines in all panels show log SFR = a log M_* + b fits obtained for Sc galaxies. The correlation is very similar in the three panels, with a logarithmic slope α = 0.77 and zero point of b = −7.66. These values are indistinguishable from those obtained by Renzini & Peng (2015) for the whole SDSS sample. This coincidence is not surprising because Sc, along with Sbc, are the galaxies that contribute the most to the local star formation rate density (Sec. 5.1), being the ones that produce the ridge line in the MSSF relation.

As is clear from Fig. 4, the spread in SFR at fixed M_* is related to galaxy morphology. Table 2 lists the slopes and zero points obtained for subsamples of fixed Hubble type. The slopes steepen systematically from 0.34 for Sa to 0.94 for Sd galaxies. This range is essentially the same as the 0.4–1 quoted by Speagle et al. (2014) as resulting from different selection criteria. The flattening for the early types also explains why many works obtain a flattening of the MSSF relation at increasing M_* (e.g. Brinchmann et al. 2004; Peng et al. 2010). It is clear in Fig. 4 that the bending in the main sequence, at least in our sample, is produced by the inclusion of large bulges, such as those in Sa and S0, and also E, where the star formation is already quenched or in the process of being quenched. These galaxies (Sa, S0, and E) are the most massive ones in our sample, but they contribute little to the cosmic star formation (as we will see in Sec. 5.1), as they are clearly off below the MSSF.

Fig. 4 shows that the three alternative cuts defined in the previous section produce practically identical MSSF when galaxies later than Sa are considered. The differences in SFR between the panels become significant in the high M_* and low SFR regime typical of early type galaxies. Note that the masses are the same from panel to panel, since all spaxels contribute to M_* . What changes is the number of spaxels entering the computation of SFR of each galaxy, hence the differences in the total rate. In practice we obtain a more extended quenched cloud in the left than in middle and right panels. This happens because the W_Hα-based cuts eliminate most E and several S0 and Sa galaxies altogether, while xy > 3.4% is not as restrictive. This again suggests that our estimation of the SFR in E and S0 is uncertain, and our method only provides an upper limit to the real SFR.

Table 2. Parameters of log SFR(M_* yr^{-1}) = a log M_(M_*) + b fits of the global MSSF for galaxies of different morphologies. They are obtained for panel (a) in Fig. 4. For convenience, the corresponding SFR for a 10^{10} M_ galaxy is also listed (in M_ yr^{-1}). Note that the slope is significantly smaller in Sa that in later spirals because most of the Sa galaxies are off the MSSF.

| morph. | Sa   | S0   | Sb   | Sbc  | Sc   | Sd   |
|--------|------|------|------|------|------|------|
| slope   | 0.34 | 0.65 | 0.71 | 0.77 | 0.94 |
| zero-point | −3.87 | −6.83 | −7.05 | −7.66 | −9.12 |
| log SFR(M_* = 10^{10} M_) | −0.47 | −0.33 | −0.05 | −0.04 | 0.28 |

5. Radial structure of the recent star formation

We now present a series of results related to spatially resolved SFR measurements of CALIFA galaxies. We focus on the radial structure of the star formation rate surface density, Σ_{SFR} (also referred to as the intensity of star formation), and the local specific star formation rate, Σ_{SFR}/μ_.*.

Using pyCASSO, we obtain, for each galaxy, 2D maps of the recent SFR computed as in equation 1 with R_{S} = 32 Myr. Each 2D map is then azimuthally averaged to obtain the radial variation of the Σ_{SFR}. Only spaxels that meet the criterion of xy > 3.4% are included in the azimuthal average. Elliptical aperture ΔR = 0.1 HLR in width are used to extract the radial profiles, with ellipticity and position angle obtained from the moments of the S635 Å flux image. We express the radial distance in units of HLR to allow comparison of the profiles of individual galaxies, and to produce stacks as a function of Hubble type and/or stellar mass.

5.1. Radial profiles of Σ_{SFR} and the role of morphology

Fig. 5 shows azimuthally averaged radial profiles of Σ_{SFR} stacked by Hubble type. The upper-left panel shows the results for all the seven morphological classes together.
All spirals show $\Sigma_{\text{SFR}}(R)$ decreasing with radial distance, with a typical gradient (measured in the central 1 HLR) $\Delta \log \Sigma_{\text{SFR}} \approx -0.78$ dex/HLR. Interestingly, the $\Sigma_{\text{SFR}}(R)$ at any radius falls within a relatively tight range of values. At $R = 1$ HLR our average $\Sigma_{\text{SFR}}$ is $20 M_{\odot}$ Gyr$^{-1}$ pc$^{-2}$, with a dispersion of 0.13 dex between spirals of different Hubble type. This is about one to two orders of magnitude smaller than the global $\Sigma_{\text{SFR}}$ measured in starbursts and local Lyman break analogs (Heckman et al. 2005), but consistent with the value obtained by Schiminovich et al. (2007) for a complete sample of GALEX star forming galaxies.

The plot also illustrates how E and S0 are clearly distinct from the spirals. Their radial profiles are flat (except for some slight increase at the center of S0). The $\Sigma_{\text{SFR}}$ at 1 HLR is $\sim 1 M_{\odot}$ Gyr$^{-1}$ pc$^{-2}$, a 20-fold decrease from spirals (maybe more given that our estimates of SFR for early types are probably upper limits).

Each of the other panels in Fig. 5 shows the radial profile of $\Sigma_{\text{SFR}}$ for each Hubble type, now computed with each of our three reliability cuts. As already discussed, imposing $x_Y > 3.4\%$ (solid line), $W_{H\alpha} > 3$ (dashed) or 6 Å (dotted) makes no difference for galaxies later than Sb, so much so that the three $\Sigma_{\text{SFR}}$ profiles are hardly distinguishable. The effects of the somewhat more restrictive $W_{H\alpha}$-cuts start to be noticed in Sa galaxies, become evident in S0 (factor of $\sim 2$ difference) and grow even larger in E (where the dotted and dashed lines fall off below the plot limits). As previously discussed, though some of our E galaxies do exhibit signs of recent star formation (Gomes et al. 2015c), most can be regarded as quenched systems, which retired from forming stars long ago. We note in passing that although our estimates for E and S0 are very uncertain, the typical value of $\sim 1 M_{\odot}$ Gyr$^{-1}$ pc$^{-2}$ is consistent with the global $\Sigma_{\text{SFR}}$ in early type galaxies estimated by Schiminovich et al. (2007).

The individual panels of Fig. 5 present two other lines which allow for interesting comparisons. The first is the horizontal line at $5 M_{\odot}$ Gyr$^{-1}$ pc$^{-2}$, which marks the $\Sigma_{\text{SFR}}$ of the Milky Way. This value is obtained by dividing the recent SFR of the Milky Way (MW), 1.6$M_{\odot}$ yr$^{-1}$, by the area of a disk of radius 1.2$\times$ the Galactocentric radius of the Sun, 8.33 kpc (Licquia & Newman 2015). This distance is equivalent to $\sim 2$ HLR of typical Sb-Sbc CALIFA galaxies. The results in Fig. 5 suggest that, in the inner $\sim 2$ HLR, most spirals in the main sequence have $\Sigma_{\text{SFR}}$ higher than the average $\Sigma_{\text{SFR}}$ in the Milky Way. This is not unexpected because it is known that the SFR in the MW is significantly lower than in other spirals of similar type and mass (see Kennicutt & Evans 2012) particularly the discussion around their

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4 They divide half of the total SFR (derived from the UV luminosity) by an area equal to $\pi$ HLR$^2$. 

图 5。左上角: 超新星爆发率密度（$\Sigma_{\text{SFR}}$）随半径变化的径向图，单位为 HLR。图横轴为 $5 M_{\odot}$ Gyr$^{-1}$ pc$^{-2}$，表示银河系的平均 $\Sigma_{\text{SFR}}$。只有半径小于 1 HLR 的位置的星系光度因子大于 3.4% 的光区域会包括。误差条显示了 log $\Sigma_{\text{SFR}}$ 对于所有的螺旋（黑色）和 Sb 银河系（绿色）的波动（不是不确定性）。图的其他部分：对于每个 Hubble 类型，实线、虚线和点划线分别表示通过排除 $x_Y < 3.4\%$，$W_{H\alpha} < 3$ Å，和 $W_{H\alpha} < 6$ Å，分别得到的平均径向图。灰色点划线显示 $\Sigma_{\text{SFR}}(R)$ 的变化。图的 SFR 密度图在假定常数率星形成过程中形成。
5.2. The dependence of $\Sigma_{\text{SFR}}(R)$ on stellar mass

As usual, it is difficult to disentangle the relative roles of morphology and $M_*$, but CALIFA has grown large enough a sample to attempt to tackle this issue by plain brute force statistics. Fig. 5 shows $\Sigma_{\text{SFR}}(R)$ profiles as a function of both $M_*$ and morphology. Besides the seven Hubble types we now break up the sample in six mass bins: $\log M_*(M_\odot) = 11.5–11.2, 11.2–10.9, 10.9–10.6, 10.6–10.1, 10.1–9.6$, and $9.6–9.1$. In each panel (one per $M_*$ bin), the average profile for each Hubble type is plotted if it contains more than five galaxies. These plots allow to evaluate how $\Sigma_{\text{SFR}}(R)$ changes with Hubble type for galaxies of similar mass.

An inspection of Fig. 5 shows that spirals with $M_* \lesssim 4 \times 10^{10} M_\odot$ (top panels) have very similar $\Sigma_{\text{SFR}}$ profiles. When relevant, the differences occur in the inner regions. Above this mass, the profiles start to disperse, although they are still packed in a relatively small range of $\Sigma_{\text{SFR}}$ values. This high degree of uniformity is a remarkable result taking into consideration that the sample covers all types of spirals and two orders of magnitude in galaxy mass. In Section 5.3 we speculate that this behaviour is intimately linked to the tightness of the MSSF.

In contrast, E and S0 have $\Sigma_{\text{SFR}}$ profiles well below those in spirals of similar mass. This suggests that in massive galaxies with a large spheroidal component the star formation is significantly quenched in the whole galaxy. However, this effect seems to be more relevant in the centers than in the outskirts, as suggested by the flat profiles in E and S0 in comparison with the radially decreasing $\Sigma_{\text{SFR}}(R)$ profile in spirals. Note that the most massive Sa galaxies in the sample show a bimodal behavior, with a smooth decrease of $\Sigma_{\text{SFR}}(R)$ outwards of 1 HLR, and a relative rate in the central part that is almost flat and significantly depressed with respect to spirals of later types. Again, this points out to the relevance that the formation of a big bulge may have in quenching the star formation in galaxies.

5.3. Radial structure of the local specific star formation rate

For a galaxy, the specific star formation rate is defined by $\text{sSFR} = \text{SFR}/M_*$. Overlooking trivial multiplicative factors (see equation 2), it gives a measure of the relative rate at which stars are forming now in a galaxy with respect to the past average rate. Because the relation between SFR and $M_*$ is sub-linear (e.g. Fig. 4), the sSFR declines with galaxy mass. Also, because of the tightness of the MSSF relation, star forming galaxies occupy a correspondingly tight locus in the sSFR vs. $M_*$ space, but bulge dominated galaxies display a much larger spread of sSFR at a fixed galaxy mass (Schiminovich et al. 2007; Salim et al. 2007; see also Fig. 4).

In analogy with the global sSFR, CALIFA data allow us to study the local sSFR, defined by the ratio $\Sigma_{\text{sSFR}}(R)/\mu_*$, that measures the relative rate of ongoing star formation with respect to the past in each position in a galaxy. Fig. 7 shows the results of stacking the $\text{sSFR}(R) = \Sigma_{\text{sSFR}}(R)/\mu_*(R)$ profiles by Hubble type. These profiles show a clear ranking with morphology, increasing from early to late Hubble type. We obtain, at $R = 1$ HLR, $\log \text{sSFR}(\text{Gyr}^{-1}) = -2.94$, $-2.85$, $-1.68$, $-1.34$, $-0.95$, $-0.77$, and $-0.59$ for E, S0, Sa, Sb, Sbc, Sc, and Sd bins, respectively. This ordering is preserved at any given radial distance, as is also the case with other stellar population properties such as mean stellar age, metallicity, and $\mu_*$ (González Delgado et al. 2015).

Fig. 5 showed that $\Sigma_{\text{SFR}}(R)$ profiles are very similar for all spirals, so the scaling of sSFR($R$) seen in Fig. 7 is a direct consequence of the variation of $\mu_*(R)$ with Hubble type, increasing from $\mu_*(R = 1\text{ HLR}) ≈ 100$ to $1000 M_\odot$ pc$^{-2}$, from Sd to Sa galaxies. The opposite happens for early type galaxies, with the sSFR($R$) profiles of E and S0 galaxies running well below those of Sa, while their $\mu_*(R)$ profiles are similar (González Delgado et al. 2015). The difference in this case comes from the much smaller levels of star formation in these systems.

All the galaxies have outwardly increasing sSFR profiles. Fig. 7 shows that in spirals sSFR($R$) grows faster with radius in the inner 1 HLR than outwards, probably signaling the bulge-

Figure 7. As the upper-left panel of Fig. 5 but for the local specific star formation rate, $\text{sSFR}(R) = \Sigma_{\text{sSFR}}(R)/\mu_*(R)$. The error bar shows the 1σ dispersion in log sSFR for Sb galaxies. The grey-dashed line at $\text{sSFR} = 0.1$ Gyr$^{-1}$ marks the value adopted by Peng et al. (2010) as a threshold to separate star forming galaxies from quiescent systems.
disk transition. Assuming that the central 0.1 HLR is dominated by the bulge and that the disk dominates outside 1 HLR, we can compare the sSFR values in these two morphological components through a ratio like $s_{\text{SFR}}(R = 0.1)/s_{\text{SFR}}(R = 1.5)$. For early type spirals (S0, Sa, Sb) this exercise results in that the sSFR of bulges is on average 0.40 dex smaller than in the disks. The difference is larger, 0.60 dex, for Sbc, while for later later types (Sc, Sd, with their small on non-existent bulges) it decreases to 0.24 dex. The sample dispersions around these values is $\sim 0.3$ dex.

As in the case of the global sSFR, the local one can also be expressed as a characteristic time-scale of star formation, $\tau(R) = s_{\text{SFR}}(R)^{-1}$ that, independently of IMF and cosmology, tells the period of time that the system needs to build its current stellar mass forming stars at the present rate $^{5}$ Measured at $R = 1$ HLR, $\tau$ ranges from 12.6 Gyr in Sbc to 5 Gyr in Sd galaxies. Early type spirals (Sa, Sb), S0, and E would all need more than the Hubble time to build their mass at their current SFR.

The dashed grey-black line in Fig. 7 at $s_{\text{SFR}} = 0.1$ Gyr$^{-1}$ marks the value adopted by Peng et al. (2010) as a threshold to separate star forming galaxies from quiescent systems. This line also marks the sSFR that galaxies should have to build their mass at the present rate during a Hubble time (approximated to 10 Gyr). The comparison of 0.1 Gyr$^{-1}$ with the sSFR profiles indicates that Sd, Sc, and the disks of Sbc are very actively forming new stars, while Sa and Sb galaxies and the bulges of Sbc, although still forming stars, are evolving to quiescent systems.

Finally, E and S0 have $s_{\text{SFR}}(R)$ values 10–100 times smaller than 0.1 Gyr$^{-1}$, with a steep increase outwards. This suggests that quenching in these galaxies has progressed inside-out.

6. Discussion

The central goal of this paper, the one embodied in its very title, was fulfilled in the previous section with the results on the radial profiles of $\Sigma_{\text{SFR}}$ and sSFR for galaxies along the Hubble sequence (Figs. 5 to 7). In this final part we go beyond this point and examine a few related issues. First we take advantage of the

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5 This standard reading of $\tau = s_{\text{SFR}}^{-1}$ actually neglects the difference between the mass turned into stars and that which stays in stars (or remnants). Because the denominator in sSFR is the current stellar mass, a rigorous definition would require a $(1-R)^{-1}$ correction for the returned mass fraction $\mathcal{R}$, not important for the discussion at this point.
need to correct for evolution over the lookback time spanned by its redshift limits.

This process yields \( \rho_{\text{SFR}} = 0.0105 \pm 0.0008 \) (random) \( M_\odot \text{yr}^{-1} \text{Mpc}^{-3} \). Fig. 8 places our estimate (black star) in the \( \rho_{\text{SFR}} \) vs. \( z \) diagram, along with other values from the literature, coming from different samples and methods. The dashed lines show the evolution of \( \rho_{\text{SFR}} \) from Madau & Dickinson (2014), Hopkins & Beacom (2006), and Fardal et al. (2007). We also include the local \( \rho_{\text{SFR}} \) from the compilation of Gunawardhana et al. (2015, 2013), and the results obtained by Pant et al. (2003) from the fossil record method applied to the SDSS data. When necessary, the literature results are scaled to a Salpeter IMF. Our estimate is smaller by 0.15 dex and higher by 0.05 dex than the values at \( z = 0 \) from Madau & Dickinson (2014) and Fardal et al. (2007), respectively. It is also in excellent agreement with the \( z < 0.1 \) estimates compiled by Gunawardhana et al. (2015, 2013), which average to 0.0109 \( M_\odot \text{yr}^{-1} \text{Mpc}^{-3} \).

Obviously, the above refers to integrated measurements, which in our case tantamounts to collapsing all our 11894 radial points into a single number. To better explore our data Fig. 8 also shows the contribution to the overall \( \rho_{\text{SFR}} \) from the different morphological types, plotted as stars (color coded by their morphology). It is clear that Sbc, Sc, and Sd galaxies dominate the \( \rho_{\text{SFR}} \) budget. Together they contribute ~75% of \( \rho_{\text{SFR}} \), despite accounting for only ~24% of the stellar mass volume density of the local Universe (\( \rho_\star \), computed following the same methodology). In contrast, Sa and Sb galaxies contribute ~22% to \( \rho_{\text{SFR}} \) and ~33% to \( \rho_\star \), while E and S0 add less than 2% to \( \rho_{\text{SFR}} \) but 43% to \( \rho_\star \).

In terms of spatial origin, 53% of \( \rho_{\text{SFR}} \) comes from the regions outwards of 1 HLR, 29% from 0.5 < \( R < 1 \) HLR, and 18% from the inner 0.5 HLR. In contrast, the \( \rho_\star \) budget for these same regions are 40, 25 and 35%, respectively. Most of the ongoing star formation thus occurs outside the centers, in disk-dominated regions, while the stellar mass is more evenly distributed with radius. If we take as reference the half mass radius (HMR), which is typically 0.8x the HLR (González Delgado et al. 2015), we find that only 35% of \( \rho_{\text{SFR}} \) comes from the regions inside the central 1 HMR, suggesting again that most of the star formation density comes from the disk-dominated regions.

6.2. The birthrate parameter

It is often useful to consider the SFR in relation to some fiducial value, instead of in absolute units. A classical example is the birthrate parameter, \( b \), that measures the current SFR of a system with respect to its lifetime average, \( \langle \text{SFR}\rangle_{\text{cosmic}} \) (Kennicutt 1989b, Scalo & Struck-Marcell 1986). This parameter conveniently separates galaxies with declining SF rates (\( b < 1 \)) from those with SF increasing (\( b > 1 \)) from past to present. \( b \) and SFR are related by

\[
b = \text{SFR} / \langle \text{SFR}\rangle_{\text{cosmic}} = s\text{SFR} \ t_\odot (1 - \mathcal{R})
\]

where \( t_\odot \) is the time over which the galaxy has formed stars\(^7\) and \( \mathcal{R} \) denotes the fraction of the mass initially turned into stars which is returned to the interstellar medium by stellar evolution. In practice, \( b = 10.08 \text{sSFR(Gyr}^{-1}) \) for \( t_\odot = 14 \text{Gyr} \) and (1-\( \mathcal{R} \)) = 0.72 (average over our sample and the Salpeter IMF assumed in the models).

\( t_\odot = t_f(z) - t_{\text{form}} \), where \( t_f(z) \) is the Hubble time at redshift \( z \) and \( t_{\text{form}} \) is the time of formation.
A volume-corrected value of $b$ representative of the local Universe can be obtained from

$$b' = \frac{\sum_i SFR_i V_{max}^{-1}}{\sum_i (SFR)_cosmic V_{max}^{-1}} \quad (3)$$

We find that $b' = 0.39 \pm 0.03$ (random). Put in words, the present-day Universe is forming stars at a little over 1/3 of its past average rate.

As for $\rho_{SFR}$ (Section 6.1), though useful, this one-number-summary of the star formation history of the Universe as a whole averages over the richness of information in CALIFA data. Our spatially resolved observations allows for definitions of $b$ that take into account its variation within galaxies [Cid Fernandes et al. 2013], the simplest of which is

$$b(R) = \frac{\Sigma_{SFR}(R)}{\langle \Sigma_{SFR}(R) \rangle_{cosmic}} \quad (4)$$

This radial profile $b(R)$ behaves exactly as the global $b$ of equation 2. There is, however, a relevant assumption implicit in this comparison of past and present as a function to radius, namely, that (statistically) stars do not move too far from their birthplaces along their lives.

Fig. 9 shows our results for $b(R)$ for our seven Hubble types. Clear and systematic trends are identified with both radial distance and morphology. First, $b(R)$ increases outwards, as expected from the inside-out growth of galaxies [Pérez et al. 2013; González Delgado et al. 2014b; Sánchez-Blázquez et al. 2014; Sánchez et al. 2014; González Delgado et al. 2015]. Secondly, $b(R)$ scales in amplitude with Hubble type, increasing from early to late spirals. Sd and Sc galaxies are currently forming stars faster than in the past at all radii. The disks ($R > 1$ HLR) of Sbc galaxies also show $b(R) > 1$, but their bulges are forming stars at lower rates than in the past. Sb and earlier types have $b(R) < 1$ throughout their disks and bulges.

Finally, we note that spheroids (E, S0, and the inner regions of early type spirals, presumably associated to bulges) all have $b < b'$. Star formation has thus stopped (or been quenched) sometime ago. Most regions in Sa have $b(R) < 0.39$, so, even though these galaxies are still forming stars, they are located in the transition between the MSSF and the quenched cloud.

### 6.3. The local main sequence of star formation

CALIFA is ideally suited to investigate the roles of global and local properties controlling the MSSF. In fact, using the spatially resolved $H\alpha$ flux of more than 500 CALIFA galaxies, Cano-Díaz et al. (2016) have recently found that the $H\alpha$-based $\Sigma_{SFR}$ correlates with the stellar mass surface density, $\mu_*$, and that the slope and dispersion of this local MSSF are similar to those of the global SFR-$M_*$ relation. A local MSSF relation has also been reported by Wuyts et al. (2013) in a sample of massive star-forming galaxies at $z \sim 1$ through spatially resolved $H\alpha$ images provided by HST. Section 4 presented our version of the global MSSF (see Fig. 4). Here we use our radial profile data to investigate the local relation.

Fig. 10 plots $\Sigma_{SFR}(R)$ against $\mu_*(R)$ for the nearly 12 thousand radial bins in our 416 galaxies. The plot is ultimately a collection of 416 $\Sigma_{SFR}(R)$ profiles where the radial coordinate is replaced by $\mu_*(R)$. Clearly, our starlight-based $\Sigma_{SFR}(R)$ and $\mu_*(R)$ values correlate. Dotted diagonals mark lines of constant sSFR. An eye-ball comparison of these lines with the data already hints that, like the global one, the local MSSF is sublinear.

Individual points in the left panel of Fig. 10 are color coded according to the galaxy morphology. Large white circles show the mean $\Sigma_{SFR}$ in 0.2 dex wide bins in $\mu_*$. The scatter around this mean relation is visibly related to morphology, as further illustrated by the mean relations obtained for Sa and Sc galaxies, drawn as blue and orange circles, respectively. The increase in $\Sigma_{SFR}$ at fixed $\mu_*$ from early to late types is another manifestation of our earlier finding that the sSFR(R) profiles scale with Hubble type (Fig. 7).

### Table 3. Parameters of log $\Sigma_{SFR}(M_\odot \, yr^{-1} \, pc^{-2}) = \alpha \log \mu_*(M_\odot/pc^2) + \beta$ fits to the local MSSF to spirals of different types.

| morph. | All | Sa | Sb | Sbc | Sc | Sd |
|--------|-----|----|----|-----|----|----|
| $\alpha$ | 0.70 | 0.60 | 0.68 | 0.70 | 0.79 | 0.85 |
| $\beta$ | -0.55 | -0.70 | -0.64 | -0.32 | -0.41 | -0.39 |
| $\alpha'$ | 0.84 | 0.87 | 0.79 | 0.78 | 0.89 | 0.80 |
| $\beta'$ | -0.85 | -1.45 | -0.93 | -0.50 | -0.60 | -0.30 |

8 Units of $M_\odot \, yr^{-1} \, pc^{-2}$ and $M_\odot/pc^2$ are assumed throughout.
For the whole data set we obtain $\alpha = 0.70 \pm 0.01$ and $\beta = -0.53 \pm 0.02$, with an rms dispersion of 0.27 dex. We have also carried out fits weighting each point by the $V_{\max}$, value of its host galaxy\textsuperscript{9} which gives the slope and zero point the status of being representative of the local Universe. The parameters for this alternative fit are $\alpha' = 0.84 \pm 0.01$ and $\beta' = -0.85 \pm 0.03$. This fit is shown as a dashed black-grey line in the right panel of Fig. 10 which repeats our local MSSF, but now coloring each radial bin of each galaxy by its contribution to the total SFR cosmic density in the local Universe ($\rho_{\text{SFR}}$).

These fits describe well the local MSSF as a whole, but completely overlook the evident role of morphology. It is thus more appropriate to fit the relation for different Hubble types, in analogy with what was done in Table 2 for the global MSSF. Table 3 lists the $\alpha$ and $\beta$ values obtained subdividing the sample in morphology. Coefficients for the $V_{\max}$-weighted fits ($\alpha'$ and $\beta'$) are also given. Dashed blue-grey and orange-grey lines in the right panel of Fig. 10 show the fitted relations for Sc and Sa galaxies, respectively.

Inspection of the results in Table 3 shows that, as anticipated by a visual assessment of the local MSSF, slopes are indeed fairly similar for all types, while $\beta$ increases monotonically from early to late types. In all cases we obtain $\alpha < 1$. While the mixture of morphological types certainly explains part of the sub linearity of both the global and local MSSF when lumping all sources together, this result indicates that the local MSSF is sub linear even for fixed Hubble type. Our values of $\alpha(\alpha') = 0.68 (0.79)$ for Sb and 0.79 (0.89) for Sc galaxies bracket the slope of 0.72 derived by Cano-Díaz et al. (2016) for the Hα-based local MSSF relation.

Our own previous work has shown that $\mu_*$ is an effective tracer of local stellar population properties. Both mean stellar ages (González Delgado et al. 2014b) and metallicities (González Delgado et al. 2014a) correlate well with $\mu_*$, and this work shows that $\Sigma_{\text{SFR}}$ also follows this pattern.

These previous studies reveal that the overall balance between local ($\mu_*$-driven) and global ($M_*$-driven) effects varies with the location within the galaxy. While in disks $\mu_*$ regulates the mean stellar ages and metallicities, it plays a minor role in spheroids (bulges and elliptical galaxies), whose chemical enrichment happened much faster and earlier than in disks. How does the local MSSF relation found in this work fit into this general scheme?

On the one hand, we have seen that the local MSSF relation is mostly a disk phenomenon. In fact, it points to a density dependence of the SFR law akin to that proposed by Schmidt (1959) and Kennicutt (1998), where the gas density sets the rate of $\Sigma_{\text{SFR}}$. Gas content is an obvious candidate hidden variable in this context (Roberts & Haynes 1994; Tacconi et al. 2013). Alternatively (or complementarily), the modulation of the $\Sigma_{\text{SFR}}$-$\mu_*$ relation with Hubble type may reflect the effect of a “morphological quenching”. In González Delgado et al. (2015) we have found that, for the same $M_*$, early type galaxies are older than later types, both globally and in the disk, and that this ranking is maintained with radial distance. This gradual age change from spheroidals to Sa and to late spirals reflects the changes in...
change of sSFR with Hubble type, and can be interpreted as a consequence of the mechanism building the bulge. The steep potential well induced by the formation of a large spheroid component stabilizes the disk, cutting the supply of the gas and preventing its local fragmentation into bound, star-forming clumps (Martig et al. 2009). This effect should thus be more significant in E and S0, and gradually decrease from Sa to Sb. Later types, Sc and Sd, where the bulge (if present) may be formed by secular processes, may not be affected by this morphological quenching.

6.4. The relation between local and global MSSFs

The results reported throughout this paper give plenty of material to explore in relation with galaxy structure and evolution studies. In this final section we develop some simple math relating the local and global MSSF relations.

The global (i.e., spatially integrated) SFR and stellar mass of a galaxy relate to the local properties through

\[
\text{SFR} = 2\pi \int \frac{\Sigma_{\text{SFR}}(R) \, dR}{\Sigma_{\text{SFR}}(R_0)} \, s_0
\]

where we have denoted HLR by \(R_0\) for convenience, and

\[
\mu_s = \int \frac{\mu_s(R) \, dR}{\mu_s(R_0)}
\]

are shape factors of order unity. Equations 5 and 6 lead to

\[
\text{SFR} = \frac{s_0 \Sigma_{\text{SFR}}(R_0)}{\mu_s(R_0)} \mu_\star(R_0)
\]

which predicts the global MSSF relation in terms of spatially resolved properties.10

Direct integration of the profiles yields a \(s_0/\mu_s\) ratio of typically 0.9 ± 0.4 for our spirals (average and dispersion), and a very weak (\(\propto M_\star^{-0.07}\)) trend with mass. Relevant deviations from a linear global MSSF must therefore come from variations of \(s\text{SFR}(R_0) = \Sigma_{\text{SFR}}(R_0)/\mu_\star(R_0)\) with \(M_\star\).

Fig. 7 shows that sSFR\(R_0\) increases systematically towards later type spirals, indicating an anti correlation with stellar mass and hence a sub-linear predicted global MSSF. More quantitatively, recalling that \(\Sigma_{\text{SFR}} \propto \mu_\star^\alpha\) from our local MSSF relation, and that \(\mu_\star(R_0) \propto M_\star^\gamma\), with \(\gamma \sim 0.5\) (González Delgado et al. 2014b), the predicted relation goes as \(\text{SFR} \propto M_\star^{\gamma + \alpha - 0.07}\). For \(\alpha\) between 0.70 and 0.84 (Table 3), and correcting for the mild trend of \(s_0/\mu_s\) with mass, the predicted logarithmic slope of the global MSSF is in the 0.78–0.85 range, in good agreement with Renzini & Peng (2015) and Cano-Díaz et al. (2016).

We close by noting that it is plausible to conclude from this analysis that the sub-linearity of the local MSSF (\(\alpha < 1\)) is what causes sub-linearity of the global MSSF11. A caveat in this tempting local \(\rightarrow\) global argument is that it uses \(\mu_\star\) to trace the local SFR density, whereas gas, not stars, is the actual fuel of star formation. We thus postpone further analysis of this issue to future work involving gas density estimates.

7. Summary and conclusions

We analyzed the stellar population properties of 416 galaxies, observed by CALIFA at the 3.5m telescope in Calar Alto, to investigate the trends of the recent star formation rate with radial distance and as a function of Hubble type. The sample includes ellipticals, S0, and spirals all the way from Sa to Sd, covering a stellar mass range from \(10^7\) to \(7 \times 10^{11}\)\(M_\odot\) (for a Salpeter IMF). A full spectral fitting analysis was performed using the starlight code and a combination of SSP spectra from González Delgado et al. (2005) plus Vazdekis et al. (2010). Our pycasso pipeline was used to process the spectral fitting results to produce maps of the recent star formation rate (SFR, averaged over the last 32 Myr), and the stellar mass surface density (\(\mu_\star\)). For each galaxy, the maps are azimuthally averaged to produce radial profiles (in units of the half light radius, HLR) of the SFR surface density, \(\Sigma_{\text{SFR}}(R_\star)\), and the corresponding local specific SFR, \(s_{\text{SFR}}(R_\star) = \Sigma_{\text{SFR}}(R_\star)/\mu_\star(R_\star)\). Variations of the traditional birthrate parameter, \(b\), are obtained to compare the present and the past SFR at different radial positions. The radial profiles are stacked as a function of Hubble type and of galaxy mass to identify the main trends.

Our main results are:

1. Spiral galaxies have declining \(\Sigma_{\text{SFR}}(R)\) profiles, with a relatively tight range of \(\Sigma_{\text{SFR}}\) values at any given radial distance. At \(R = 1\) HLR the \(\Sigma_{\text{SFR}}\) is typically \(20\, M_\odot\, \text{Gyr}^{-1}\, \text{pc}^{-2}\), with a factor of two dispersion. Spirals with \(M_\star \leq 4 \times 10^{10}\, M_\odot\) have \(\Sigma_{\text{SFR}}(R)\) profiles that are very similar and independent of Hubble type and galaxy mass. Above \(4 \times 10^{10}\, M_\odot\) the \(\Sigma_{\text{SFR}}(R)\) profiles are slightly more dispersed. This is a remarkable result taking into consideration that the sample covers two orders of magnitude in \(M_\star\) and all Hubble types. Ultimately, it is the constancy of \(\Sigma_{\text{SFR}}\) that, coupled to the \(\mu_\star - M_\star\) relation, makes the MSSF a tight sequence.

2. In contrast, E and S0 galaxies have \(\Sigma_{\text{SFR}}(R)\) that are at all radii significantly depressed with respect to spirals, with flat \(\Sigma_{\text{SFR}} \sim 1\, M_\odot\, \text{Gyr}^{-1}\, \text{pc}^{-2}\) profiles, with a large uncertainty.

3. Expressed in units of the lifetime averaged SFR intensity at each location, the present \(\Sigma_{\text{SFR}}(R)\) is currently lower in E, S0, and early type spirals (Sa and Sb), but higher in later spirals (Sc and Sd). Sbc galaxies seem to be the transition type in which “bulges” (central ~1 HLR) have already suppressed/quenched their star formation activity, as in Sa and Sb, but their disks are still forming new stars at a rate similar to the past.

4. The local sSFR = \(\Sigma_{\text{SFR}}/\mu_\star\) shows radial profiles that increase outwards and scale with Hubble type, from Sa to Sd. This behavior is preserved at any given R. This quantity, that relates locally the present and the past star formation rate, is orders of magnitude smaller in E and S0 than in spirals. The characteristic time scale of star formation given by sSFR in spirals ranges from 12.6 Gyr in Sbc to 5 Gyr in Sd galaxies. Early type spirals (Sa, Sb) and spheroidals (E, S0) would

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10 Eq. 10 can be written more compactly as sSFR = \(\frac{\mu_s}{s_0}\)sSFR\(R_0\), where the left-hand-side is the global (spatially integrated) SFR.

11 We clarify that the sub-linearity we refer to here is not that resulting from mixing galaxies of different morphologies in a same sample, but the one found when fitting the global MSSF at fixed Hubble type (i.e., the \(a < 1\) slopes in Table 2).
need more than a Hubble time to build their current stellar mass at their recent SFR.

5. The slope of $\Sigma_{\text{SFR}}(R)$ in the inner 1 HLR is steeper than outwards. This behavior with radial distance suggests that galaxies are quenched inside-out, and that this process is faster in the central part (dominated by the bulge) that in the disk.

6. The CALIFA sample is well suited to compute the SFR density in the local universe, with a value $\rho_{\text{SFR}} = 0.0105 \pm 0.0008$ (random) $M_\odot \, \text{yr}^{-1} \, \text{Mpc}^{-2}$ (for a Salpeter IMF), in excellent agreement with previous estimates from completely different methods and data. We find the majority of the star formation at $z = 0$ to take place in Sbc, Sc, and Sd galaxies, with all $b > 1$, dominate the present star formation of the Universe.

7. The volume average birthrate parameter, $b' = 0.39$, suggests that the present day Universe is forming stars at $\sim 1/3$ of its past average rate. E, S0, and the bulge of early type spirals have $b < 0.39$, thus contributing little to the present star formation rate of the Universe. The disks (regions outside 1 HLR) of Sbc, and Sc, and Sd galaxies, all with $b > 1$, dominate the present star formation of the Universe.

8. Galaxy mass and morphology, in particular the formation of a spheroidal component, play a relevant role in depressing/quenching the star formation in galaxies. Galaxies dominated by the spheroidal component, E and S0 in our sample, are all quiescent. Disk dominated galaxies (Sbc, Sc, Sd) are very actively forming stars with a rate per unit mass that decreases with $M_*$.

There is tight relation between the local values of $\mu_*$ and $\Sigma_{\text{SFR}}$, defining a local main sequence of star forming regions with slope $\sim 0$ and a scatter strongly related to Hubble type. This relation is tighter than the global main sequence relation between SFR and $M_*$ once morphology-related offsets are accounted for. This suggests that local processes are important in determining the star formation in a galaxy, possibly due to a density dependence of the SFR law. The shut down of the star formation is more related with global processes, such as the formation of a spheroidal component. These findings agree with our previous analysis that showed that the mean stellar ages and metallicity are mainly governed by local processes ($\mu_*$ driven) in disks, and by global processes in spheroids.

Thanks to the uniqueness of CALIFA data and the homogeneity of our analysis, we were able to, for the first time, characterize the radial structure of the star formation rate along the Hubble sequence. This octogenarian sequence, by the way, has once again demonstrated its usefulness as a way to organize the Hubble sequence. This octogenarian sequence, by the way, has once again demonstrated its usefulness as a way to organize the Hubble sequence. We thank the support of the IAA Computing group, and to the referee for useful comments.

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References

Abazajian, K., Adelman-McCarthy, J. K., Agüeros, M. A., et al., 2003, AJ, 126, 2081
Asari, N. V., Cid Fernandes, R., Statitska, G., et al., 2007, MNRAS, 381, 263
Ascasibar, Y. & Sánchez Almeida, J. 2011, MNRAS, 415, 2471
Baldry, I. K., Glazebrook, K., Brinkmann, J., et al., 2004, ApJ, 608, 661
Bica, E. 1988, A&A, 195, 76
Bica, E., Allon, D., & Schmitt, H. R. 1994, A&A, 283, 805
Binietti, L., Magris, C. G., Statitska, G., & Bruzual, A. G. 1994, A&A, 292, 13
Blanton, M. R., Hogg, D. W., Bahcall, N. A., et al., 2003, ApJ, 592, 819
Blanton, M. R. & Moustakas, J. 2009, ARA&A, 47, 159
Brinchmann, J., Charlot, S., White, S. D. M., et al., 2004, MNRAS, 351, 1151
Bruzual, G. & Charlot, S. 2003, MNRAS, 344, 1000
Bryan, J. J., Owens, M. S., Robotham, A. S. G., et al., 2015, MNRAS, 447, 2857
Bundy, K., Bershady, M. A., Law, D. R., et al. 2015, ApJ, 798, 7
Cappellari, M. & Copin, Y. 2003, MNRAS, 342, 345
Cappellari, M., Emsellem, E., Krajnović, D., et al., 2011, MNRAS, 413, 813
Cassisi, J., Ascasibar, Y., Gavilán, M., et al., 2015, MNRAS, 451, 888
Catalán-Torrejón, C., Gil de Paz, A., Castillo-Morales, A., et al., 2015, A&A, 584, A87
Chabrier, G. 2003, PASP, 115, 767
Chang, Y.-Y., van der Wel, A., da Cunha, E., & Rix, H.-W. 2015, ApJS, 219, 8
Charbonnel, C., Meynet, G., Maeder, A., Schaller, G., & Schaerer, D. 1993, A&AS, 101, 415
Cid Fernandes, R. & González Delgado, R. M. 2010, MNRAS, 403, 780
Cid Fernandes, R., González Delgado, R. M., García Benito, R., et al., 2014, A&A, 561, A130
Conroy, C. 2013, ARA&A, 51, 393
Daddi, E., Dickinson, M., Morrison, G., et al., 2007, ApJ, 670, 156
Elbaz, D., Daddi, E., Le Borgne, D., et al., 2007, A&A, 468, 33
Elbaz, D., Dickinson, M., Hwang, H. S., et al., 2011, A&A, 533, A119
Faber, S. M., Willner, C. N. A., Wolf, C., et al. 2007, ApJ, 665, 265
Fardal, M. A., Katz, N., Weinberg, D. H., & Davé, R. 2007, MNRAS, 379, 985
Flores-Fajardo, N., Morisset, C., Statitska, G., & Binette, A. 2015, MNRAS, 451, 2182
Gallagher, III, J. S., Hunter, D. A., & Tutukov, A. V. 1984, ApJ, 284, 544
García-Benito, R., Vílchez, J. M., et al., 2015a, A&A, 588, 81
García-Benito, R., Mateus, A., Vílchez, J. M., et al., 2015, MNRAS, 358, 363
García-Benito, R., Pérez, E., García Benito, R., et al., 2013, A&A, 557, A86
García-Benito, R., Statitska, G., Mateus, A., & Vale Asari, N. 2011, MNRAS, 415, 1687
García-Benito, R., Mateus, A., Vílchez, J. M., et al., 2015, A&A, 576
González Delgado, R. M., Cerviño, M., Martins, L. P., Leitherer, C., & Hauschildt, P. H. 2005, MNRAS, 357, 945
González Delgado, R. M., Cid Fernandes, R., García-Benito, R., et al. 2014a, A&A, 571, L16
González Delgado, R. M., Cid Fernandes, R., Pérez, E., et al. 2004, ApJ, 605, 127
Appendix A: Dependence of SFR on SSP models

In order to evaluate to what extent our results depend on the choice of SSP models, we compare the properties derived with two bases: Base $GMe$, i.e., the one used in the main text and briefly described in Sec. 3.1, and base $CBe$, used in several earlier works by our group, and fully described in González Delgado et al. (2015). In short, this base is built out of a preliminary update of the Bruzual & Charlot (2003) models (Bruzual 2007, private communication), from which we draw $N_\star = 246$ elements with 41 ages (from 0.001 to 14 Gyr) and six metallicities ($\log Z/Z_\odot = -2.3, -1.7, -0.7, -0.4, 0$, and $+0.4$). The evolutionary tracks are those collectively referred to as Padova 1994 by Bruzual & Charlot (2003), and the IMF is that of Chabrier (2003). Compared to $GMe$, base $CBe$ differs in evolutionary tracks, IMF, and metallicity range.

We make two types of comparisons in this appendix: (i) global (galaxy wide) quantities, such as the present day and initial stellar masses, and the total SFR; and (ii) radial averages of $\mu_\star$, $A_V$, $\Sigma_{\text{SFR}}$, $\Sigma_{\text{SFR}}/\mu_\star$, and $x_Y$ for up to a maximum 30 of points for each galaxy (corresponding to $R = 0$–3 in steps of 0.1 HLR).

Fig. A.1 shows the results, with base $GMe$ values in the x-axis and $CBe$ ones in the y-axis. Each panel shows a one-to-one line, as well as the mean ($\Lambda$) and standard deviation ($\sigma$) of the difference $\Delta \equiv \text{property}(CBe) - \text{property}(GMe)$.

On average, $GMe$-based $M_\star$ and $\mu_\star$-values are $\sim 0.26$ dex higher than the corresponding $CBe$-based values, reflecting the different IMF used. Discounting this offset, the two values of stellar mass and mass surface density agree to within 0.06 and 0.11 dex, respectively. In terms of the initial mass that is converted into stars ($M_{\text{ini}}$) there is a difference of 0.12 dex between the two bases and a dispersion of 0.06 dex. Again, the difference reflects the change of IMF between the two bases. Note that $\Delta \log M_\star$ is higher than $\Delta \log M_{\text{ini}}$ because the returned fraction $R$ also differs from one base to the other ($R = 0.28$ and 0.48 for $GMe$ and $CBe$, respectively).

Due to the IMF difference, the SFR should be lower for $CBe$ than for $GMe$. This is in fact the result (Fig A.1d), but the difference is only 0.07 dex, lower than what we would expect due to the change of IMF. This implies that besides the IMF, there are differences in the SFH between $GMe$ and $CBe$ and/or in stellar extinction. The latter explanation does not hold, since $A_V$ is very similar in the two sets of models, with an offset of only $\Delta = 0.03$ mag and dispersion $\sigma = 0.06$ mag. However, we note that there is an important difference between the light fraction in populations younger than 32 Myr. On average, $x_Y$ is 0.18 dex higher with $CBe$ than $GMe$. This explains why the SFR with $CBe$, although lower than with $GMe$, is not a full factor of $\sim 1.7$ lower, as expected due to the change of IMF.

This change in SFH, and in particular in $x_Y$, does not produce any significant effect in the radial distribution of the star formation rate intensity, $\Sigma_{\text{SFR}}(R)$. The two sets of values are well correlated (Fig. A.1p), with a tiny difference of $\Delta = -0.05$ dex (lower in $CBe$ than in $GMe$), and a dispersion $\sigma = 0.15$ dex. The offset of $\Sigma_{\text{SFR}}/\mu_\star$ between the two bases is $\Delta = 0.23$ dex, reflecting mainly the offset in $\mu_\star$ due to the IMF (Fig. A.1p).
Fig. A.1. Comparison of several stellar population properties as obtained with the bases GMe (x-axis) and CBe (y-axis). The average difference between the property in the y and x-axis is labeled as $\Delta$ in each panel, and its standard deviation as $\sigma$. Panels (a), (b), and (d) show the galaxy mass and SFR, with galaxies colored by their Hubble type. In the other panels, the values of the property measured every 0.1 HLR are compared, and the color indicates the density of points in a logarithmic scale.