A quantitative spectral analysis of 14 hypervelocity stars from the MMT survey

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ABSTRACT

Context. Hypervelocity stars (HVSs) travel so fast that they may leave the Galaxy. The tidal disruption of a binary system by the supermassive black hole in the Galactic center is widely assumed to be their ejection mechanism.

Aims. To test the hypothesis of an origin in the Galactic center using kinematic investigations, the current space velocities of the HVSs need to be determined. With the advent of Gaia’s second data release, accurate radial velocities from spectroscopy are complemented by proper motion measurements of unprecedented quality. Based on a new spectroscopic analysis method, we provide revised distances and stellar ages, both of which are crucial to unravel the nature of the HVSs.

Methods. We reanalyzed low-resolution optical spectra of 14 HVSs from the MMT HVS survey using a new grid of synthetic spectra, which account for deviations from local thermodynamic equilibrium, to derive effective temperatures, surface gravities, radial velocities, and projected rotational velocities. Stellar masses, radii, and ages were then determined by comparison with stellar evolutionary models that account for rotation. Finally, these results were combined with photometric measurements to obtain spectroscopic distances.

Results. The resulting atmospheric parameters are consistent with those of main sequence stars with masses in the range 2.5–5.0 M⊙. The majority of the stars rotate at fast speeds, providing further evidence for their main sequence nature. Stellar ages range from 90 to 400 Myr and distances (with typical 1σ-uncertainties of about 10–15%) from 30 to 100 kpc. Except for one object (B 711), which we reclassify as A-type star, all stars are of spectral type B.

Conclusions. The spectroscopic distances and stellar ages derived here are key ingredients for upcoming kinematic studies of HVSs based on Gaia proper motions.

Key words. stars: distances – stars: early-type – stars: fundamental parameters

1. Introduction

Runaway stars are young early-type stars with unusual kinematics that have been found outside of star-forming regions (OB associations, open clusters). Surveys of blue stars have even revealed their presence in the Galactic halo, into which they have probably been injected from the Galactic disk by a powerful ejection mechanism. Many decades ago now, two ejection mechanisms were proposed. In the binary supernova ejection scenario (Blaaauw 1961), the secondary star of a close binary system is ejected when the primary explodes as a core-collapse supernova. Alternatively, dynamical interactions between (binary) stars in young, open clusters can give large kicks to the stars involved in a close encounter (Poveda et al. 1967).

The kinematically most extreme stars, the hypervelocity stars (HVSs), are believed to be ejected by the supermassive black hole in the Galactic center via the tidal disruption of a binary system (for a review see Brown 2015). This so-called Hills mechanism (Hills 1988) can accelerate stars to ~1000 km s⁻¹, that is, well beyond the Galactic escape velocity, making them gravitationally unbound to the Milky Way. After the first serendipitous discoveries (Brown et al. 2005; Hirsch et al. 2005; Edelmann et al. 2005), a systematic survey covering 12,000 square degrees of the sky led to the discovery of almost two dozen unbound HVSs of late B type with masses between 2.5 and 4 M⊙ (Brown et al. 2014). Besides the unbound HVSs, the Hills mechanism is also predicted to produce an equal number of lower velocity, i.e., probably bound, HVSs (Bromley et al. 2009). Indeed, Brown et al. (2014) identified 16 such stars whose Galactic rest-frame velocities exceed 275 km s⁻¹. The velocity distribution of young stars in the Galactic halo is therefore expected to be produced by an overlap of the three different acceleration mechanisms listed above, at least for the lower-velocity tail of HVSs (<700 km s⁻¹) where extreme runaway stars start to contribute (Heber et al. 2008a; Przybilla et al. 2008a; Irrgang et al. 2010; Silva & Napiwotzki 2011). In order to distinguish between the scenarios, kinematic studies have to be used (Kenyon et al. 2014). Proper motions measured with the Hubble Space Telescope (HST) turned out to be not accurate enough to calculate trajectories with sufficiently small uncertainties to pinpoint the origin in the Galactic plane (Brown et al. 2015). With its second data release, Gaia now provides more accurate proper motions. Therefore, it is of utmost importance to determine spectroscopic distances that are as accurate and precise as possible in order to exploit the excellent quality of Gaia’s proper motions.
The MMT HVS survey by Brown et al. (2014) discovered 38 late B-type HVSs, 16 of which are considered to be bound to the Galaxy. We selected the 14 most interesting ones, that is, those stars which have proper motions measured by HST. The corresponding MMT spectra cover the very blue optical range from 3600 to 4500 Å, which nicely traces the confluence of the Balmer series. However, the modeling of this region is challenging because a proper treatment of the dissolution of the hydrogen levels is required. We used a new generation of model atmospheres and synthetic spectra which account for this effect (Sect. 2) to reanalyze the MMT spectra of Brown et al. (2014), allowing us to derive effective temperatures and surface gravities with significantly improved accuracy (Sect. 3). Additionally, radial and projected rotational velocities are determined during our simultaneous fitting procedure. The latter are of particular importance in order to distinguish between blue horizontal-branch (BHB) and B-type main sequence stars, which populate the same region in the Hertzsprung-Russell-diagram and are, thus, indistinguishable by means of effective temperature and surface gravity alone (Heber et al. 2008b). High projected rotational velocities are indicative of a main sequence nature. By comparison with evolutionary tracks, we derived stellar masses and ages (Sect. 4) and, in combination with photometry, spectroscopic distances (Sect. 5). We conclude with a brief glimpse into the Gaia era (Sect. 6).

3. Atmospheric parameters and projected rotational velocities

The quantitative analysis strategy as described by Irrgang et al. (2014) was applied to simultaneously fit the entire spectral range to derive $T_{\text{eff}}$, $\log(g)$, the radial velocity $v_{\text{rad}}$, and the projected rotational velocity $vsin(i)$. An exemplary fit to one of the MMT spectra of HVS 9 is shown in Fig. 2. The results are listed in Table 1 and visualized in Fig. 3. While for most of the stars in the sample, the effective temperatures agree quite well with the previous results by Brown et al. (2015), there are three objects (HVS 4, HVS 12, B 485) that show significant differences of $\sim$1000 K and one (B 711) of $\sim$2000 K. Given the wealth of spectral lines in its spectrum, the program star B 711 turned out to be an early A-type instead of a later B-type star. The new surface gravities do not agree well with previous results. However, this is expected because the more sophisticated treatment of level dissolution in our new models alters the profiles as well as the confluence of the Balmer lines. Our surface gravities scatter less and nicely match the range predicted by stellar evolution models for the main sequence, allowing us to exploit the region around the Balmer jump, which is an important indicator for the surface gravity, for quantitative spectral analysis, which is particularly important for the analysis of the MMT spectra given their spectral range (3600–4500 Å).

Fig. 1. Comparison of synthetic spectra ($T_{\text{eff}} = 12000$ K, $\log(g) = 4.4$, solar composition) calculated with the original Atlas12 code (thin black line) and our modified version including level dissolution (thick red line). The proper implementation of this effect allows us to exploit the region around the Balmer jump, which is an important indicator for the surface gravity, for quantitative spectral analysis, which is particularly important for the analysis of the MMT spectra given their spectral range (3600–4500 Å).

2. Model atmospheres and synthetic spectra

Synthetic spectra for B-type stars are calculated from the structure of a line-blanketed, plane-parallel, homogeneous, and hydrostatic model atmosphere in local thermodynamic equilibrium (LTE) computed with the Atlas12 code (Kurucz 1996). Departures from LTE are allowed for by calculating atomic population numbers using the Detail code (Giddings 1981) to solve the coupled radiative transfer and statistical equilibrium equations. The synthetic spectrum is then computed with Surface (Giddings 1981) making use of the departure coefficients and the best line-broadening data available. This so-called ATLAS, DETAIL, SURFACE (ADS) or hybrid LTE/non-LTE approach is described in detail by Przybilla et al. (2011). To model spectra of A-type stars and cooler, we make use of the pure LTE spectrum synthesis code SYNTH (Kurucz 1993).

Recently, the ATLAS12, DETAIL, SURFACE, and SYNTH codes have been improved by one of us (A. Irrgang). The occupation probability formalism (Hummer & Mihalas 1988) for hydrogen and ionized helium – following the description given by Hubeny et al. (1994) – as well as state-of-the-art line broadening tables for hydrogen (Tremblay & Bergeron 2009) have been implemented. Both are of particular importance to model the Balmer jump as demonstrated in Fig. 1. Moreover, non-LTE effects on the atmospheric structure are now considered in the sense that departure coefficients for hydrogen and helium are passed back from DETAIL to ATLAS12 to refine the atmospheric structure iteratively. Among other things, this ensures a more realistic representation of the spectral energy distribution (SED).

A grid of synthetic spectra with solar chemical composition based on the ADS approach has been computed for effective temperatures $T_{\text{eff}}$ ranging from 9000 to 16000 K in steps of 250 K and surface gravities $\log(g)$ between 3.0 and 4.6 in steps of 0.2. To account for cooler stars, a similar grid based on ATLAS12 and SYNTHE has been computed covering effective temperatures between 7000 and 10 000 K in steps of 200 K.
rotational velocity of HVS 10 and HVS 12 is consistent with zero, which could be explained by a low inclination of the rotational axis.

Three stars of the sample have previously been studied with high-resolution spectra. Przybilla et al. (2008b) used the ADS approach to analyze HVS 7. Their parameters (\(T_{\text{eff}} = 12\,000 \pm 500\,\text{K}, \log(g) = 3.8 \pm 0.1, \nu \sin(i) = 55 \pm 2\,\text{km s}^{-1}\)) agree very well with our values presented in Table 1. Similarly, the parameters derived by López-Morales & Bonanos (2008) for HVS 8 (\(T_{\text{eff}} = 11\,000 \pm 1000\,\text{K}, \log(g) = 3.75 \pm 0.25, \nu \sin(i) = 260 \pm 70\,\text{km s}^{-1}\)) and by Brown et al. (2012) for HVS 5 (\(T_{\text{eff}} = 12\,000 \pm 350\,\text{K}, \log(g) = 3.89 \pm 0.13, \nu \sin(i) = 133 \pm 7\,\text{km s}^{-1}\)) are consistent with ours. This good agreement gives us confidence that the spectral coverage and resolution of the MMT spectra are sufficient to derive accurate parameters.

4. Evolutionary masses and stellar ages

Figure 3 shows the comparison between derived atmospheric parameters and predictions of rotating stellar models of solar metallicity for the main sequence (Georgy et al. 2013). The resulting atmospheric parameters are consistent with the stars being main sequence stars with masses between 2.5 and 5.0 \(M_\odot\). Stellar masses \(M\), ages \(\tau\), radii \(R\), luminosities \(L\), and ratios of actual angular velocity to critical velocity \(\Omega/\Omega_{\text{cr}}\) are derived by interpolation of the evolutionary tracks and are listed in Table 1. Lacking other indicators, we use the projected rotational velocity (multiplied by a statistical factor of \(4/\pi\) based on the simple assumption of isotropic \(\sin(i)\) values) as proxy for the equatorial rotation and, hence, for stellar rotation.

5. Spectroscopic distances and interstellar reddening

Photometric measurements allow additional parameters to be derived, namely the stellar angular diameter and the interstellar reddening. The angular diameter, in turn, grants access to the distance because the stellar radius is already known (see Sect. 4). We constructed SEDs from optical (SDSS-DR14: Blanton et al. 2017) and infrared (UKIDSS-DR9: Lawrence et al. 2007; ALLWISE: Cutri et al. 2014) photometry. Synthetic SEDs (based on the atmospheric parameters derived via spectroscopy; see Table 1) were then calculated with our improved version of ATLAS12 and fitted to the observed ones by adjusting the angular diameter and the color excess \(E(B-V)\) (for details see Heber et al. 2018). The extinction curve by Fitzpatrick (1999) was used to compute the wavelength-dependent reddening factor \(10^{-0.4E(\lambda)}\), with which the flux has to be multiplied, from the fitting parameter \(E(B-V)\) and the fixed extinction parameter \(R_V = A(V)/E(B-V) = 3.1\). As an example, Fig. 4 shows the result of such an exercise in the case of HVS 9. The resulting values for the color excess and stellar distance are listed in Table 1. The error budget is dominated by the uncertainties of the atmospheric parameters, in particular by \(\log(g)\). The resulting distances range from 10 to 100 kpc and have typical 1\(\sigma\)-uncertainties of about 10–15%.

6. The Gaia era

Gaia astrometry will have an enormous impact on stellar astrophysics and Galactic astronomy. The mission will provide proper motions of unprecedented accuracy. For instance, a comparison between HVS proper motions measured with HST and those measured with Gaia is given by Marchetti et al. (2018) for predicted end-of-mission performance and by Brown et al. (2018) for the second data release. For the first time, it will be possible to derive significant constraints on the place of origin as well as on the ejection mechanism of HVSs. In order to derive precise transversal velocities, we aimed at determining spectroscopic distances for 14 HVSs by reanalyzing their spectra from the MMT HVS survey using models with improved spectral synthesis of the Balmer line series. Besides revised atmospheric parameters and radial and projected rotational velocities, we provide more realistic stellar masses and ages. The resulting atmospheric distances
Table 1. Atmospheric and stellar parameters of the program stars.

| Object                          | $T_{\text{eff}}$ (K) | $\log(g)$ (cgs) | $v_{\sin(i)}$ (km s$^{-1}$) | $r_{\odot}$ (M$\odot$) | $\tau$ (Myr) | $\log(L/L_\odot)$ | $R$ (R$\odot$) | $\Omega/D_{\text{eq}}$ | $E(B-V)$ (mag) | $d$ (kpc) | 1$\sigma$ |
|--------------------------------|----------------------|-----------------|-----------------------------|-------------------------|-------------|-------------------|----------------|-------------------|----------------|-----------|-----------|
| HVS 1 (SDSS J090744.99+024506.9) | 11 120 +280         | 3.85 +0.13      | 829.7 +5.5                 | 160 +37                 | 3.2 +0.3   | 272 +29           | 2.22 +0.20     | 3.5 +1.1         | 0.75 +0.05       | 0.099 +0.087 | 99.3 +7.52 | +5.52    |
| HVS 4 (SDSS J091301.01+305119.8) | 13 280 +370         | 3.89 +0.16      | 604.6 +5.7                 | 138 +23                 | 4.0 +0.4   | 150 +14           | 2.59 +0.21     | 3.8 +1.6         | 0.64 +0.03       | 0.005 +0.006  | 78.3 +15.35 | +9.67    |
| HVS 5 (SDSS J091759.48+672238.3) | 12 530 +340         | 4.20 +0.17      | 542.5 +5.9                 | 131 +36                 | 3.3 +0.3   | 97 +10            | 2.09 +0.20     | 2.4 +1.4         | 0.61 +0.03       | 0.109 +0.022 | 31.2 +9.63 | +10.23   |
| HVS 6 (SDSS J110557.45+093439.5) | 12 190 +320         | 4.19 +0.17      | 619.3 +5.9                 | 125 +23                 | 3.1 +0.3   | 142 +14           | 2.04 +0.13     | 2.3 +1.5         | 0.59 +0.03       | 0.033 +0.005  | 57.7 +19.11 | +22.63   |
| HVS 7 (SDSS J113312.12+010824.9) | 12 800 +270         | 3.93 +0.17      | 524.0 +5.9                 | 88 +22                  | 3.5 +0.3   | 185 +14           | 2.39 +0.13     | 3.4 +1.8         | 0.31 +0.07       | 0.006 +0.007  | 48.2 +17.11 | +12.61   |
| HVS 8 (SDSS J094214.04+203322.1) | 10 960 +360         | 4.04 +0.17      | 499.6 +5.9                 | 282 +22                 | 2.9 +0.3   | 226 +16           | 1.98 +0.13     | 2.7 +1.7         | 0.95 +0.05       | 0.026 +0.006  | 37.2 +15.11 | +12.61   |
| HVS 9 (SDSS J102137.08+005234.8) | 12 030 +310         | 3.91 +0.17      | 622.0 +6.0                 | 261 +23                 | 3.5 +0.3   | 175 +15           | 2.35 +0.13     | 3.5 +1.9         | 0.95 +0.05       | 0.106 +0.012  | 66.6 +16.05 | +13.10   |
| HVS 10 (SDSS J120337.85+180230.4) | 11 040 +340         | 4.18 +0.17      | 462.0 +5.9                 | 55 +22                  | 2.7 +0.3   | 210 +15           | 1.82 +0.13     | 2.2 +1.6         | 0.29 +0.09       | 0.047 +0.008  | 54.2 +13.56 | +12.94   |
| HVS 12 (SDSS J110509.60+031550.7) | 11 170 +300         | 4.34 +0.17      | 545.0 +5.9                 | 0 +23                   | 2.5 +0.3   | 90 +10            | 1.64 +0.13     | 1.8 +1.2         | 0.00 +0.00       | 0.076 +0.006  | 51.7 +13.17 | +16.95   |
| HVS 13 (SDSS J110524.31+000133.9) | 11 370 +340         | 4.11 +0.17      | 568.1 +5.9                 | 166 +33                 | 2.9 +0.3   | 200 +14           | 1.97 +0.21     | 2.5 +1.7         | 0.76 +0.07       | 0.037 +0.012  | 95.2 +14.35 | +15.69   |
| B 434 (SDSS J112244.37+025002.8) | 10 190 +250         | 3.85 +0.17      | 445.5 +5.9                 | 101 +33                 | 2.8 +0.3   | 402 +14           | 2.01 +0.13     | 3.3 +1.9         | 0.54 +0.05       | 0.072 +0.013  | 40.5 +12.22 | +13.47   |
| B 485 (SDSS J110118.82+302028.1) | 15 200 +360         | 3.89 +0.17      | 422.9 +5.9                 | 69 +24                  | 4.8 +0.3   | 94 +14            | 2.91 +0.13     | 4.1 +1.7         | 0.35 +0.03       | 0.018 +0.005  | 33.3 +13.87 | +11.75   |
| B 711 (SDSS J142001.94+124404.8) | 9 170 +280         | 3.71 +0.17      | 271.0 +5.9                 | 0 +24                   | 2.8 +0.3   | 393 +14           | 1.97 +0.13     | 3.9 +1.9         | 0.00 +0.00       | 0.009 +0.002  | 28.5 +10.63 | +13.67   |
| B 733 (SDSS J144955.58+103515.4) | 10 750 +300         | 4.23 +0.17      | 350.8 +5.9                 | 223 +24                 | 2.6 +0.3   | 123 +16           | 1.71 +0.13     | 2.1 +1.7         | 0.95 +0.05       | 0.024 +0.004  | 9.9 +2.41  | +1.41    |

Notes. Uncertainties in the atmospheric parameters are the quadratic sums of statistical (99%−confidence limits) and systematic uncertainties. Systematic uncertainties cover only the effects induced by additional variations of 2% in $T_{\text{eff}}$ and 0.1 in $\log(g)$ and are formally taken to be 99%−confidence limits (see Irrgang et al. 2014 for details). Uncertainties in the stellar parameters cover the effects induced by varying $T_{\text{eff}}$ and $\log(g)$ in the given uncertainty ranges and, therefore, are also formally taken to be 99%−confidence limits. For comparison, distance uncertainties are also given as 1$\sigma$ uncertainties, i.e., as 68%−confidence limits, by dividing the 99%−confidence limits by a factor of 2.576. Photometric uncertainties are included in the error budget for the distance. The atmospheric parameters of B 711 are based on ATLAS12/SYNTHIE.
reduce the systematic uncertainties. High-resolution spectroscopy is required to study the chemical composition of the stars. Last but not least, our derived stellar ages can be compared to kinematic times of flight to further constrain the origin of the HVSs.

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