Free-space data-carrying bendable light communications

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Bendable light beams have recently seen tremendous applications in optical manipulation, optical imaging, optical routing, micromachining, plasma generation and nonlinear optics. By exploiting curved light beams instead of traditional Gaussian beam for line-of-sight light communications, here we propose and demonstrate the viability of free-space data-carrying bendable light communications along arbitrary trajectories with multiple functionalities. By employing 39.06-Gbit/s 32-ary quadrature amplitude modulation (32-QAM) discrete multi-tone (DMT) signal, we demonstrate free-space bendable light intensity modulated direct detection (IM-DD) communication system under 3 different curved light paths. Moreover, we characterize multiple functionalities of free-space bendable light communications, including bypass obstructions transmission, self-healing transmission, self-broken trajectory transmission, and multi-receiver transmission. The observed results indicate that bendable light beams can make free-space optical communications more flexible, more robust and more multifunctional. The demonstrations may open a door to explore more special light beams enabling advanced free-space light communications with enhanced flexibility, robustness and functionality.

In recent years, bendable light beams have received a great deal of attention because of their tremendous application potential in a diversity of fields such as optical manipulation1–3, optical imaging4,5, optical routing6, micromachining7, plasma generation8 and nonlinear optics9–12. Bendable light beams are a novel class of electromagnetic wave associated with a localized intensity maximum that propagates along a curved trajectory. Since the initial work studying Airy beam solutions of the paraxial wave equation propagating along parabolic trajectories13–15, more general classes of bendable light beams have been reported including Mathieu beams along elliptical trajectories and Weber beams along parabolic trajectories16–18. Airy beam is one type of nondiffracting beams, which can maintain its wavefront during transmission just like Bessel beam19–27. In contradistinction with the Bessel beam, the Airy beam possesses the properties of self-acceleration in addition to nondiffraction and self-healing, which propagates along a parabolic trajectory. In addition to Airy beam, bendable light beams can also reconstruct their wavefront, and continue propagate along the preset trajectory28,29. To exploit the advantage of bendable light beams for different applications, one need to bend the light along arbitrary trajectories. An efficient way to realize arbitrary curved light beam is based on the caustic method, which associates the desired trajectory with an optical light caustic. This method can be implemented in both real space and Fourier space30–35.

Recently, Airy beams were employed for free space information transfer36–38. However, they did not take full advantage of the bendable light beams to realize more functionalities. Here, we also use bendable light beams in free-space optical communications. In traditional free-space optical communications, the optical path is always a straight line connecting the transmitter and receiver. However, there are sometimes obstructions between the transmitter and receiver, which makes communication failure. By using curved light beams for free-space optical communications, one can easily navigate around the obstructions by setting appropriate trajectories. Besides, bendable light beams are nondiffracting beams. When coming through an obstruction, they can reconstruct their wavefront and continue to propagate along the preset trajectories. Moreover, by designing proper trajectories, one can send information to multiple users and avoid unwanted users. Thus, by employing bendable light beams in free-space optical communications, it will make the communication system more flexible and robust.

By simply using the phase only spatial light modulation, we realize bendable light beams along arbitrary trajectories including self-broken trajectory. By employing 39.06-Gbit/s 32-ary quadrature amplitude modulation (32-QAM) discrete multi-tone (DMT) signal, we successfully demonstrate free-space bendable light intensity modulated direct detection (IM-DD) communication system using 3 different curved light paths. Moreover, we also characterize the transmission performance under 4 different conditions: (i) bypass obstructions

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communication; (ii) self-healing communication; (iii) self-broken trajectory communication; (iv) movable multi-receiver communication.

Results

Concept and principle. Figure 1 illustrates the concept and principle of free-space bendable light communications. Here shows one example of free-space data-carrying bendable light communication system from one side of a circuit board to the other side. Firstly, by carefully designing the specific phase pattern for spatial light modulation via optical light caustic method, one can build arbitrarily curved light paths, which makes the communication system much more flexible. Secondly, in contrast to traditional Gaussian beam, the generated bendable light can also avoid or bypass existed obstructions as expected. Thirdly, the data-carrying bendable light can recover its wavefront when directly passing through the obstruction. The self-healing property of the curved light beam makes the communication system more robust. Fourthly, one can even construct a self-broken trajectory curved light beam, which can avoid unwanted users. Finally, owing to the self-healing property, the curved light can deliver the information to multi-users along the curved light path. Consequently, by employing bendable light, the free-space communication system will become more multifunctional, more flexible and more robust.

Experimental configuration. The experimental configuration used in proof-of-concept demonstration of free-space bendable light communications is shown in Fig. 2. A 39.06-Gbit/s 32-QAM DMT signal at 1550 nm from the transmitter is sent to the collimator to generate a free-space Gaussian beam with a beam diameter of 2 μm and a numerical aperture (NA) of 0.24. A polarizer (Pol.) is used for light polarization alignment with the polarization-sensitive spatial light modulator (SLM). Then the light is expended by a 5x beam expander (BE), which can illuminate the full extent of the SLM. The data-carrying bendable light is generated immediately after the SLM, which is loaded with the desired phase pattern by optical light caustic method for bendable light beam generation. In order to record the full propagating trajectory, a two lens 4-f imaging system is employed. A camera is placed after the 4-f system to record the propagation dynamics of the bendable light by moving along a motorized linear translation stages. At last, the main lobe of the curved light beam is coupled into the receiver with an optical collimator for signal detection.
Multifunction bendable light communications. We first demonstrate free-space bendable light communications along arbitrary trajectories. Three bendable light beams with different curved trajectories are successfully generated. The measured intensity distributions are depicted in Fig. 3(a–c). The propagating distance of the curved light beams are all 300 mm along the z direction. The curved light beams (BP1 and BP2) in Fig. 3(a,b) are along parabolic trajectories. The bending offset of them are both 1.4 mm. Moreover, we also generate S-shaped curved light beam (BP3), which is displayed in Fig. 3(c). The bending offset of two peaks are both 0.7 mm. From the measured intensity distributions, one can clearly find that the measured bendable light beams are in good agreement with the predesigned trajectories as marked by blue dashed lines shown in Fig. 3(a–c). Furthermore, we measure the bit-error rate (BER) performance as a function of the received optical signal-to-noise ratio (OSNR) for the three bendable light beams, as depicted in Fig. 3(d). 39.06-Gbit/s 32-QAM DMT signals are employed in the IM-DD free-space communication system. The observed OSNR penalties at a BER of $2 \times 10^{-3}$ (enhanced forward error correction (EFEC) threshold) for the three bendable light beams (BP1, BP2 and BP3) are $-0.9$ dB. The insets in Fig. 3(d) plot constellations of 32-QAM DMT signals.

We further demonstrate multiple functionalities of free-space bendable light communications. Firstly, we set obstructions along the line of sight between the transmitter and receiver, as shown in Fig. 4(a). The Gaussian beam is also considered for comparison. One obstruction (Ob1) is set at $z = 75$ mm and the other (Ob2) is set at $z = 225$ mm. The diameter of the obstructions are both 0.8 mm. We first set one obstruction (Ob1), and measure the BER performance of the S-shaped light beam (curve BP-Ob-1). Then, we set two obstructions (Ob1 and Ob2) simultaneously, and measure the BER curve of the S-shaped light beam (curve BP-Ob-2). The BER performance of both conditions are almost the same as the one without obstructions (curve BP). The observed OSNR penalties at a BER of $2 \times 10^{-3}$ are about 0.9 dB. However, for Gaussian beam with obstructions, one cannot receive enough optical power for signal detection. The BER of Gaussian beam transmission with obstructions (curve Gauss-Ob) is about 0.5, as shown in Fig. 4(a).

Secondly, we demonstrate the self-healing property of the free-space bendable light communications. An obstruction with a diameter of 0.8 mm is set at the curve path of the S-shaped bendable beam ($z = 75$ mm), as depicted in Fig. 4(b). Thus, the curved light is blocked by the obstruction. After propagation, the light reconstructs its wavefront. A receiver is placed at $z = 300$ mm to receive the self-healing data-carrying bendable light. We also measure the transmission performance of the reconstructed light (curve BP-Re), as shown in Fig. 4(b). As seen from the BER curve, one can easily find that the reconstructed light has almost the same performance with the non-blocked one (curve BP).

Thirdly, we also generate a curved light beam with self-broken trajectory, as shown in Fig. 4(c). From $z = 170$ mm to $z = 200$ mm, the main lobe of the curved light is missing, and then recovered at the end. Thus, one cannot detect the information at the broken part (from $z = 170$ mm to $z = 200$ mm). We then set the receiver at $z = 185$ mm (R1), and measure the BER performance, which is shown in the BER curve (curve BP-Break). The received BER cannot reach the EFEC Threshold. Moreover, we also measure the BER performance at $z = 300$ mm (R2), as shown in the BER curve (curve BP). The observed OSNR penalties at a BER of $2 \times 10^{-3}$ are about 1 dB, which means one can successfully receive the information at the end of the bendable light beam.

At last, we characterize the communication performance of the bendable light beam for multiple users. Owing to the self-healing property, the curved light can deliver the information to movable multiple users along the curved light path trajectory, which is not available for traditional free-space light communications. Here, we set three receivers along the light path ($z = 75$ mm (R1), 225 mm (R2), and 300 mm (R3)), which is marked in
Fig. 4(d). The measured BER performance is plotted in Fig. 4(d). The three receivers have almost the same transmission performance. The observed OSNR penalties at a BER of $2 \times 10^{-3}$ are about 0.9 dB.

Discussion

In summary, we successfully demonstrate free-space data-carrying bendable light communications. Moreover, we characterize multiple functionalities of free-space bendable light communication, including bypass obstructions transmission, self-healing transmission, self-broken trajectory transmission, and multi-receiver transmission. The observed results indicate that bendable light can make the free-space optical communication more multifunctional, more flexible and more robust. We expect this scheme to be also scalable in propagation distance and bending offset. The demonstrations may open a door to explore more special light beams and facilitate more extensive free-space light communication applications with advanced flexibility, robustness and functionality.

Method

Phase profile engineering for generating bendable light beams. The phase profile engineering for generating arbitrary curved light beams is based on the caustic method, which associates the desired trajectory with an optical light caustic. Shown in Fig. 5(a) is an example of geometric construction for generating a parabolic trajectory. The desired bendable light trajectory is defined by the curve $x = f(z)$. The goal is to determine the
Figure 5. (a) Geometric construction for generating phase profile $\varphi(x)$ from the properties of a parabolic trajectory $x = f(z)$. (b) Geometric construction for generating phase profile $\varphi(x)$ from the properties of an S-shaped trajectory.

Figure 6. Phase patterns for generating the four bendable light beams in the experiments. (a) Bendable light beam in Fig. 3(a). (b) Bendable light beam in Fig. 3(b). (c) Bendable light beam in Fig. 4(c). (d) Bendable light beams in Figs. 3(c), 4(a), 4(b) and 4(d).
corresponding spatial phase profile \( \varphi(x) \) at the plane \( z = 0 \), which can generate the desired bendable light beam as a caustic. A caustic is defined as an envelope to a group of tangents such that each point \( x \) at the \( z = 0 \) can be functionally related to a point on the caustic via a tangent of slope \( \theta \), where \( \tan(\theta) = \frac{df(z)}{dz} \). Thus, one can determine the desired phase function by integrating the phase derivative condition:

\[
\frac{d\varphi(x)}{dx} = k \sin(\theta) = k \frac{df(z)/dz}{\sqrt{1 + (df(z)/dz)^2}},
\]

where \( k \) is the wave number. By using this method, we can get the corresponding phase profile for generating bendable light.

For generating arbitrary trajectory, such as S-shaped trajectory, we can also use caustic method combining with phase grating. The geometric construction for generating an S-shaped trajectory is shown in Fig. 5(b). The phase profile \( \varphi(x) \) can be divided into two parts \( \varphi_1(x) \) and \( \varphi_2(x) \). In part 1, each point in the phase profile needs to generate two light paths with different diffraction angles. By combining the two phase distributions for generating two light paths, one can get the final phase profile of \( \varphi_i(x) \). In part 2, the phase profile \( \varphi_2(x) \) is calculated with the same method described in Fig. 5(a). Thus, by controlling the grating phase distribution of the phase profile, one can achieve arbitrary convex trajectory. The phase patterns for generating the four bendable light beams are shown in Fig. 6.

Transmitter and receiver. Intensity modulated direct detection (IM-DD) is a good candidate in inter-connect due to its low cost. Several solutions such as pulse amplitude modulation (PAM), discrete multi-tone (DMT) and carrier-less amplitude phase modulation (CAP) are proposed to satisfy high-speed signal transmission in short reach optical communications. Among these solutions, DMT is highly preferred as it inherits all advantages of OFDM signal, such as transparency to modulation formats and robustness to chromatic dispersion (CD). The implementation details of the transmitter and receiver in the experimental configuration are shown in Fig. 7.

At the transmitter, an arbitrary waveform generator (Tektronix AWG 70002) operating at 20-GSa/s is used to generate the 32-QAM DMT signal. Here the FFT size for DMT generation is 256, in which 100 subcarriers are modulated with 32-QAM data. Thus the gross bitrate is 39.06 Gbit/s. Hermitian symmetry is employed to produce real-valued DMT signal. In each frame, 20 training symbols (TS) used for the adaptive frequency domain equalization are added to the beginning of the 200 DMT symbols and a cyclic prefixes (CP) of 8 is added to each DMT symbol. An external cavity laser with 100-kHz linewidth operating at 1550 nm is used as the optical carrier. After being amplified by an electrical amplifier (EA), the DMT signal is modulated via an intensity modulator.

At the receiver side, the received signal is first re-sampled to 20-GSamples/s to match the sample rate of AWG. After that, a frame synchronization process is utilized to find the DMT frame start point. After serial-to-parallel (S/P) conversion and CP removing, FFT operation is employed to transfer the signal to the frequency domain. Then a 1-tap equalization is used to compensate the linear distortions of the system. Finally, 32-QAM de-mapping and P/S conversion are performed. The bit-error rate (BER) is obtained by error counting.

Received: 2 January 2019; Accepted: 22 May 2019;
Published online: 18 October 2019

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Acknowledgements
This work was supported by the National Natural Science Foundation of China (NSFC) under grants 11574001, 61761130082 and 11774116, the National Key R&D Program of China under grant 2018YFB1801803, the National Basic Research Program of China (973 Program) under grant 2014CB34004, the Royal Society-Newton Advanced Fellowship, the National Program for Support of Top-notch Young Professionals, the Yangtze River Excellent Young Scholars Program, the Natural Science Foundation of Hubei Province of China under grant 2018CFA048, the Key R&D Program of Guangdong Province under grant 2018B030325002, the Program for HUST Academic Frontier Youth Team under grant 2016QYTD05, the Fundamental Research Funds for the Central Universities under grant 2019kyfYRCPY037, and the Open Fund of IPOC (BUPT) under grant IPOC2018A002.

Author contributions
J.W. developed the concept and conceived the experiments. L.Z. and A.W. carried out the experiments. L.Z. and A.W. analyzed the experimental data. L.Z. and J.W. contributed to writing and finalizing the paper. J.W. supervised the project.

Competing interests
The authors declare no competing interests.

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