K2-231 b: A sub-Neptune exoplanet transiting a solar twin in Ruprecht 147

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ABSTRACT

We identify a sub-Neptune exoplanet (Rp = 2.5 ± 0.2 R⊕) transiting a solar twin in the Ruprecht 147 star cluster (3 Gyr, 300 pc, [Fe/H] = +0.1 dex). The ∼81 day light curve for EPIC 219800881 (V = 12.71) from K2 Campaign 7 shows six transits with a period of 13.84 days, a depth of ∼0.06%, and a duration of ∼4 hours. Based on our analysis of high-resolution MIKE spectra, broadband optical and NIR photometry, the cluster parallax and interstellar reddening, and isochrone models from PARSEC, Dartmouth, and MIST, we estimate the following properties for the host star: $M_⋆ = 1.01 ± 0.03 M_⊙$, $R_⋆ = 0.95 ± 0.03 R_⊙$, and $T_{\text{eff}} = 5695 ± 50$ K. This star appears to be single, based on our modeling of the photometry, the low radial velocity variability measured over nearly ten years, and Keck/NIRC2 adaptive optics imaging and aperture-masking interferometry. Applying a probabilistic mass–radius relation, we estimate that the mass of this planet is $M_p = 7_{-3}^{+5} M_⊕$, which would cause a RV semi-amplitude of $K = 2 ± 1$ m s$^{-1}$ that may be measurable with existing precise RV facilities. After statistically validating this planet with BLENDER, we now designate it K2-231 b, making it the second sub-stellar object to be discovered in Ruprecht 147 and the first planet; it joins the small but growing ranks of 23 other planets found in open clusters.

Keywords: open clusters: individual (Ruprecht 147, NGC 6774) — stars: individual: (K2-231, EPIC 219800881, CWW 93, 2MASS J19162203−1546159) — planets and satellites: detection — planets and satellites: gaseous planets

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1. INTRODUCTION

Transit and Doppler surveys have detected thousands of exoplanets, and modeling their rate of occurrence shows that approximately one in three Sun-like stars hosts at least one planet with an orbital period under 29 days (Fressin et al. 2013). Stars tend to form in clusters from the gravitational collapse and fragmentation of molecular clouds (Lada & Lada 2003), so it is natural to expect that stars still existing in clusters likewise host planets at a similar frequency. In fact, circumstellar disks have been observed in very young clusters and moving groups (2.5 to 30 Myr; Haisch et al. 2001). However, some have speculated that stars forming in denser cluster environments (i.e., the kind that can remain gravitationally bound for billions of years) will be exposed to harsher conditions than stars formed in looser associations or that join the Galactic field relatively quickly after formation, and this will impact the frequency of planets formed and presently existing in star clusters. For example, stars in a rich and dense cluster might experience multiple supernovae during the planet-forming period (the lifetime of a 10 M\textsubscript{☉} star is \(\sim 30\) Myr), as well as intense FUV radiation from their massive star progenitors that can photoevaporate disks. Furthermore, stars in denser clusters (\(\sim 0.3-30\) FGK stars pc\(^{-3}\))\textsuperscript{2} will also dynamically interact with other stars (and binary/multiple systems) at a higher frequency than more isolated stars in the field (\(\sim 0.06\) stars pc\(^{-3}\)),\textsuperscript{3} which might tend to disrupt disks and/or eject planets from their host star systems.

These concerns have been addressed theoretically and with observations (Scally & Clarke 2001; Smith & Bonnell 2001; Bonnell et al. 2001; Adams et al. 2006; Fregeau et al. 2006; Malmberg et al. 2007; Spurzem et al. 2009; de Juan Ovelar et al. 2012; Vinecke & Pfalzner 2016; Kraus et al. 2016; Cai et al. 2017), and all of these factors were considered by Adams (2010) in evaluating the birth environment of the solar system, but progress in this field necessitates that we actually detect and characterize planets in star clusters, and determine their frequency of occurrence.

1.1. Planets discovered in open clusters

Soon after the discovery of the first known exoplanet orbiting a Sun-like star (Mayor & Queloz 1995), Janes (1996) suggested open clusters as ideal targets for photometric monitoring. Two decades later, we still only know of a relatively small number of exoplanets existing in open clusters. One observational challenge has been that the majority of nearby star clusters are young and therefore their stars are rapidly rotating and magnetically active. Older clusters with inactive stars tend to be more distant and their Sun-like stars are likewise too faint for most Doppler and ground-based transit facilities. The first planets discovered in open clusters with the Doppler technique were either massive Jupiters or potentially brown dwarfs: Lovis & Mayor (2007) found two sub-stellar objects in NGC 2423 and NGC 4349; Sato et al. (2007) detected a companion to a giant star in the Hyades; Quinn et al. (2012) discovered two hot Jupiters in Praesepe (known as the “two b's in the Beehive”, one of which also has a Jupiter-mass planet in a long period, eccentric orbit; Malavolta et al. 2016) and Quinn et al. (2014) discovered another in the Hyades; finally, non-transiting hot Jupiters have been found in M67 around 3 main-sequence stars, one Jupiter was detected around an evolved giant, and 3 other planet candidates were identified (Brucalassi et al. 2014, 2016, 2017).

NASA’s Kepler mission changed this by providing high-precision photometry for four clusters (Meibom et al. 2011). Two sub-Neptune sized planets were discovered in the 1 Gyr NGC 6811 cluster, and Meibom et al. (2013) concluded that planets occur in that dense environment \((N = 377\) stars) at roughly the same frequency as in the field. After Kepler was re-purposed as K2, many more clusters were observed for \(\sim 80\) days each, and as a result many new cluster planets have been identified. Many of these are hosted by lower-mass stars that are intrinsically faint and difficult to reach with existing precision RV facilities from Earth. So far, results have been reported from K2 monitoring of the following clusters, listed in order of increasing age: Gaidos et al. (2017) report zero detections in the Pleiades (see also Mann et al. 2017a). Mann et al. (2016a) and David et al. (2016a) independently discovered a Neptune-sized planet transiting a M4.5 dwarf in the Hyades; recently Mann et al. (2017b) reported 3 Earth-to-Neptune-sized

\textsuperscript{1} As of 2017 June 9, 2950 are confirmed with 2338 additional Kepler candidates; http://exoplanets.org

\textsuperscript{2} Based on 528 single and binary members in M67 contained within 7.4 pc, and 111 members within the central 1 pc (Geller et al. 2015).

\textsuperscript{3} Based on the 259 systems within 10 pc tabulated by the Research Consortium On Nearby Stars (RECONS; Henry et al. 1997, 2006). http://www.recons.org/

\textsuperscript{4} The sub-stellar objects have minimum masses of 10.6 and 19.8 M\textsubscript{Jup}, respectively. Spiegel et al. (2011) calculate the deuterium-burning mass limits for brown dwarfs to be 11.4-14.4 M\textsubscript{Jup}, which supports a brown dwarf classification for the later object, and places the former on the boundary between regimes.
planets orbiting a mid-K dwarf in the Hyades (K2-136), while Ciardi et al. (2017) concurrently announced the Neptune-sized planet and that this K dwarf formed a binary with a late M dwarf; the system was later reported on by Livingston et al. (2017). In Praesepe, Obermeier et al. (2016) announced K2-95 b, a Neptune-sized planet orbiting an M dwarf, which was later studied by Libralato et al. (2016), Mann et al. (2017a), and Pepper et al. (2017); adding the planets found by Pope et al. (2016), Barros et al. (2016), Libralato et al. (2016), and Mann et al. (2017a), there are 6 confirmed planets (including K2-100 through K2-104) and one candidate, that were validated by Mann et al. (2017a). Finally, Nardiello et al. (2016) reported three planetary candidates in the M67 field, although all appear to be non-members.

Table A1 lists the 23 planets that have been discovered in clusters so far. Of these, 14 transit their host stars, and all but 4 of the hosts are fainter than V > 13, which makes precise RV follow-up prohibitively expensive. These hosts are all relatively young (~650 Myr) and magnetically active, and thus might still present a challenge to existing Doppler facilities and techniques. Such RV observations are required to measure masses and determine the densities of these planets.

1.2. The K2 Survey of Ruprecht 147

Ruprecht 147 was also observed by K2 during Campaign 7. Curtis et al. (2013) demonstrated that R147 is the oldest nearby star cluster, with an age of 3 Gyr at a distance of 300 pc (see also the Ph.D. dissertation of Curtis 2016). According to Howell et al. (2014), planets only a few times larger in size than Earth would be detectable around dwarfs at least as bright as V < 16, which approximately corresponds to a M0 dwarf with M = 0.6 M\odot in R147. Soon after the public release of the Campaign 7 light curves, we discovered a substellar object transiting a solar twin in Ruprecht 147 (EPIC 219388192; CWW 89A from Curtis et al. 2013), which we determined was a warm brown dwarf in an eccentric ~5 day orbit, and we announced our discovery at The 19th Cambridge Workshop on Cool Stars, Stellar Systems, and the Sun (“Cool Stars 19”) in Uppsala, Sweden (Curtis et al. 2016). Nowak et al. (2017) independently discovered and characterized this system.

Now, we report the identification of an object transiting a different solar twin in R147 (CWW 93 from Curtis et al. 2013), which we show is a sub-Neptune exoplanet. We made this discovery while reviewing and comparing light curves from various groups for our stellar rotation program (we are measuring rotation periods for R147’s FGKM dwarfs to validate and calibrate gyrochronology at 3 Gyr), and noticed a repeating shallow transit pattern spaced at ~14 days in the EVEREST light curve for K2-231 (Luger et al. 2016, 2017).

In this paper, we describe our production of a light curve, which we model to derive the properties of the exoplanet (Section 2). We also characterize the host star and check for stellar binary companionship (Section 3), and test false positive scenarios in order to statistically validate the exoplanet (Section 4).

K2-231 was also targeted by the following programs: “Statistics of Variability in Main-Sequence Stars of Kepler 2 Fields 6 and 7” (PI Guzik, GO 7016), “The Masses and Prevalence of Small Planets with K2 – Cycle 2” (PI Howard, GO 7030), and “K2 follow-up of the nearby, old open cluster Ruprecht 147” (PI Nascimbeni, GO 7056).

2. K2 LIGHT CURVE ANALYSIS

The top panel of Figure 1 shows the EVEREST light curve for EPIC 219800881 that caught our attention. We then downloaded the calibrated pixel-level data from the Barbara A. Mikulski Archive for Space Telescopes (MAST), extracted a light curve, and corrected for K2 systematic effects following Vanderburg & Johnson (2014). We confirmed the transits detected by eye with a Box-Least-Squares periodogram search (BLS, Kovács et al. 2002). The BLS periodogram identified a strong signal at a 13.844 day period with a transit depth of approximately 0.06%. We then refined the light curve by simultaneously fitting the K2 pointing systematics, a low-frequency stellar activity signal (modeled with a basis spline with breakpoints spaced every 0.75 days), and transits (using Mandel & Agol 2002 models), as described in Section 4 of Vanderburg et al. (2016). Deviating from our standard procedure of using stationary apertures, we opted to use a smaller, moving circular aperture with a radius of 9” (2.32 pixels) in order to ex-
include many nearby background stars (see Figure 3 and Table 4). The middle panel of Figure 1 shows the detrended version of our extracted light curve using the best-fit low-frequency model produced during the light curve calibration.

The determination of the physical radius of the planet candidate and size of its orbit requires an accurate characterization of the host star, which we present in Section 3. In this work, we adopt the following conventions from IAU 2015 Resolution B3 for the nominal radii for the Sun and Earth, which we apply to convert the measured transit quantities $a/R_\star$ and $R_p/R_\star$ to physical and terrestrial units (Mamajek et al. 2015; Prša et al. 2016): $1 (R)_\odot^N = 6.957 \times 10^8$ m and $1 (R)_\oplus^N = 6.3781 \times 10^6$ m, where this nominal terrestrial radius is Earth’s “zero tide” equatorial value.

We modeled the light curve with EXOFAST (Eastman et al. 2013). EXOFAST is an IDL-based transit and RV fitter for solving single planet systems, which employs the Mandel & Agol (2002) analytic light curve model, limb darkening parameters from Claret & Bloemen (2011), and accounts for the long 30 minute $K2$ cadence. EXOFAST requires prior information on the time of transit and the period of the orbit; the stellar temperature, metallicity, and surface gravity; and without radial velocities (RVs), Eastman et al. recommend fixing the orbit geometry to circular as the light curve does not provide adequate constraints on eccentricity or the argument of periastron.

Next, we modeled the light curve following the procedure applied in the Zodiacal Exoplanets In Time program (ZEIT), described in Mann et al. (2016a, 2017a,b), which employs model light curves generated with the BAsic Transit Model cAlculatioN code (batman; Kreidberg 2015) and the quadratic limb-darkening law sampling method from Kipping (2013). We also accounted for the 30 minute cadence, and assigned a Gaussian prior on the stellar density of $\rho_\star = 1.17\pm0.12 \rho_\odot$ derived from our estimates of the star’s mass and radius. The posterior distributions of the various model parameters were sampled with the affine-invariant MCMC code emcee (Foreman-Mackey et al. 2013).

In Table 1, we report the median values for each parameter, and errors as the 84.1 and 15.9 percentile values (i.e., $1\sigma$ for a Gaussian distribution). Figure 2 plots the posterior distributions and correlations for a subset of transit-fit parameters resulting from our MCMC analysis. Note that duration and inclination are not fit, but are derived from the stellar density and impact parameter. The eccentricity and argument of periastron are weakly constrained, which is common for long-cadence data, especially when lacking RV data. Likewise, the stellar density posterior is essentially a reflection of the adopted prior, as it encapsulates the uncertainty in eccentricity. Because the posteriors are not necessarily Gaussian or symmetric, it is possible that the median values reported here for one set of values do not perfectly translate to that of others. Similarly, the plotted model is the best-fit (i.e., highest likelihood), which is not necessarily the same as the median value.

The bottom panel of Figure 1 shows this same light curve phase-folded according to the 13.841901 day period along with the model solution from the ZEIT procedure. As we will discuss later in Section 4, there is a star $\sim4^\prime$ south of K2-231 and fainter by $\sim4$ mag. We corrected the light curve for the dilution of the transit caused by this star by assuming that this star contributes a flat signal with relative flux of $\approx1/40$, which increases the derived radius by a few percent. With the ZEIT procedure, we find that K2-231 b has a radius of $R_p = 2.48 \pm 0.2 R_\oplus$. For comparison, EXOFAST returned $R_p = 2.42 \pm 0.14 R_\oplus$, which is consistent to 0.3 $\sigma$. The EXOFAST uncertainty appears lower because we forced it to fit a circular orbit whereas eccentricity was allowed to float in the ZEIT procedure.

Note to readers of this preprint: We will include our final light curve as “data behind the figure” in the journal edition; a CSV file is also posted in this arXiv submission. The first column is BJD$-2454833$, the second column is the flux, and the third column is detrended flux using the best-fit low-frequency model.

3. PROPERTIES OF THE HOST STAR

Curtis et al. (2013) demonstrated that K2-231 is a member of Ruprecht 147, and therefore it should share the properties common to the cluster, including a spectroscopic metallicity of $[\text{Fe/H}] = +0.10$ dex (Curtis 2016), an age of 3 Gyr, a distance of 295 pc based on the distance modulus of $m - M = 7.35$, and an interstellar extinction of $A_V = 0.25$ mag, derived from fitting Dartmouth isochrone models (Dotter et al. 2008) to the optical and NIR color–magnitude diagrams (CMD). We estimate the mass and radius of this star with a combination of spectroscopic and photometric data, and then argue that this star is likely single (i.e., not a stellar binary).
Figure 1. K2 light curves for K2-231: (a) The EVEREST light curve used to visually identify the transiting object, with the transits marked as short, red vertical lines at the bottom of the figure. (b) Our refined and detrended light curve, extracted with a 9″ circular moving aperture while simultaneously fitting the pointing systematics, activity signal, and transits following Vanderburg et al. (2016), with the transits similarly marked. (c) Our detrended light curve, phase-folded according to the 13.842 day period, along with the model for highest likelihood solution from the ZEIT transit-fit procedure (see Table 1), sampled at the times of observation according to the 30 minute integration cadence (red). Our calibrated light curve and the detrended version are both available in the online journal as a comma-separated values file.
Table 1. Stellar and Planetary Properties for K2-231b

| Parameter                                      | Value       | 68.3% Confidence | Source                      |
|------------------------------------------------|-------------|-------------------|-----------------------------|
| Interval Width                                |             |                   |                             |
| Other Designations: EPIC 219800881, NOMAD 0742–0804492, CWW 93, 2MASS J19162203–1546159 |
| **Basic Information**                         |             |                   |                             |
| Right Ascension [hh:mm:ss]                    | 19:16:22.04 | ...              | Gaia DR1                    |
| Declination [dd:mm:ss]                        | −15:46:16.37 | ...              | Gaia DR1                    |
| Proper Motion in RA [mas yr⁻¹]                | −0.5        | 1.0              | HSOY                        |
| Proper Motion in Dec [mas yr⁻¹]               | −25.0       | 1.0              | HSOY                        |
| Absolute Radial Velocity [km s⁻¹]             | 41.576      | 0.004 ± 0.1      | HARPS                       |
| V magnitude                                   | 12.71       | 0.04             | APASS                       |
| Distance to R147 [pc]                         | 295         | 5                | C13                         |
| Visual Extinction (AV) for R147 [mag]         | 0.25        | 0.05             | C13                         |
| Age of R147 [Gyr]                             | 3           | 0.25             | C13                         |
| **Stellar Properties**                        |             |                   |                             |
| M⋆ [M⊙]                                       | 1.01        | 0.03             | Phot+Spec+Iso               |
| R⋆ [R⊙]                                       | 0.95        | 0.03             | Phot+Spec+Iso               |
| log g⋆ [cgs]                                  | 4.48        | 0.03             | Phot+Spec+Iso               |
| T eff [K], adopted                            | 5695        | 50               | Phot+Spec+Iso               |
| Spectroscopic Metallicity                     | +0.14       | 0.04             | SME                         |
| R147 Metallicity                              | +0.10       | 0.02             | SME                         |
| v sin i [km s⁻¹]                              | 2.0         | 0.5              | SME                         |
| Mt. Wilson S HK                                | 0.208       | 0.005            | Section 3.4                 |
| Mt. Wilson log R′ HK                          | −4.80       | 0.03             | Section 3.4                 |
| **Planet Properties**                         |             |                   |                             |
| Orbital Period, P [days]                      | 13.841901   | 0.001352         | Transit                     |
| Radius Ratio, R P / R⋆                        | 0.0239      | +0.0020          | Transit                     |
| Scaled semimajor axis, a/R⋆                   | 27.0        | +4.8             | Transit                     |
| Transit impact parameter, b                   | 0.55        | +0.23            | Transit                     |
| Orbital inclination, i [deg]                  | 88.6        | +0.9             | Derived                     |
| Transit Duration, t [hours]                   | 2.94        | +2.02            | Derived                     |
| Time of Transit T 0 [BJD-2400000]              | 57320.00164 | +0.00354         | Transit                     |
| Planet Radius R P [R⊙]                       | 2.5         | 0.2              | Converted                   |

Note—Coordinates are from Gaia DR1 (Gaia Collaboration et al. 2016a); proper motions are from HSOY (Altmann et al. 2017); the RV is the weighted mean for the 6 HARPS RVs and the uncertainties represent the precision and accuracy, respectively, where the accuracy is an approximation of the uncertainty in the IAU absolute velocity scale (Table 6); the V magnitude is from APASS (Henden et al. 2016); the distance, age, and extinction are from Curtis et al. (2013); the cluster metallicity was derived from SME analysis (Valenti & Piskunov 1996) of 7 solar analog members of R147 (Curtis 2016); the metallicity and projected rotational velocity were derived from SME analysis of the MIKE spectrum; the adopted stellar mass, radius, temperature, and surface gravity were derived by analyzing the available spectroscopic and photometric data together with isochrone models (see Section 3); the transit parameters are the median values and the 68% interval from the posterior distributions resulting from our MCMC analysis, except for the transit duration and inclination which are derived from from the stellar density and impact parameter. The planetary radius, measured relative to the stellar radius, is converted to terrestrial units using values for the Earth and Sun radius from IAU 2015 Resolution B3. Chromospheric activity indices were measured from Hectochelle spectra following principals described in Wright et al. (2004).
Figure 2. Results of the ZEIT MCMC transit-fitting procedure. This corner plot shows posterior distributions and correlations of a subset of the transit-fit parameters, including the ratio of planetary to stellar radius $R_p/R_*$, eccentricity $e$, impact parameter $b$, and stellar density in solar units. The blue-dashed lines indicate the median values for each distribution; the red-dashed line shows the mode for the eccentricity plot. The shaded regions mark the 68%, 95%, and 99.7% contours of the MCMC posteriors.

3.1. Spectroscopy

On 2016 July 15, we used the MIKE spectrograph (Bernstein et al. 2003) on the 6.5 m Magellan Clay Telescope at Las Campanas Observatory in Chile to acquire a spectrum of K2-231 with the 0.70″ slit, corresponding to a spectral resolution of $R = 42,000$; the per-pixel signal-to-noise ratio is $S/N = 130$ and 208 at the peaks of the Mg i b and 5940–6100 Å orders, respectively. We also observed 6 other solar analogs in R147 at $R = 42,000$ and 20 solar analogs in the field at $R = 55,000$ (including 18 Sco and the Sun as seen from reflection off of the dwarf planet Ceres, which we observed with both resolution settings). We reduced these spectra with the Carnegie Python pipeline (“CarPy”), which performs the standard calibrations (i.e., overscan, bias, flat field, sky background, and scattered light corrections, and mapping in wavelength using Thorium–Argon lamp spectra).

We analyzed these spectra with version 423 of Spectroscopy Made Easy (SME; Valenti & Piskunov 1996) following the Valenti & Fischer (2005) procedure. Adopting stellar properties for the field stars from Brewer et al. (2016), that sample spans $T_{\text{eff}} = 5579$ to 5960 K, log $g = 4.10$ to 4.50 dex, and [Fe/H] = $-0.09$ to $+0.14$ dex. We find median offsets and standard deviations between the Brewer et al. (2016) properties and our values of $T_{\text{eff}} = -11$, 27 K, log $g = -0.04$, 0.035 dex, and [Fe/H] = $-0.016$, 0.02 dex. These numbers illustrate our ability to reproduce the Brewer et al. (2016) results with different data and a different SME procedure (we do not employ the expanded spectral range and line list of Brewer et al. 2015, 2016), and they are all within the SME statistical uncertainties quoted by Valenti & Fischer (2005) of 44 K, 0.06 dex, and 0.03 dex, respectively.

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14 http://code.obs.carnegiescience.edu/mike
Regarding the sample of 7 solar analogs in R147, after applying the offsets, we find \([\text{Fe/H}] = +0.10 \pm 0.04\) dex, where the uncertainty is the standard deviation of the sample; the standard deviation of the mean is \(\pm 0.02\) dex and is reported in Table 1. While the R147 dispersion is higher than measured in the field star sample relative to the Brewer et al. (2016) metallicities, this is probably due to the typically lower signal-to-noise ratios and spectral resolutions of the R147 spectra (the stars are much fainter) compared to the field stars taken from Brewer et al. (2016), and not intrinsic to the sample. For a separate project, Iván Ramírez measured stellar properties for five of these solar analogs with the same or similar MIKE spectra (since his work, we have collected higher quality data for particular stars for our analysis described here). Following Ramírez et al. (2013), he employed a differential analysis with respect to the Sun by enforcing the excitation/ionization balance of iron lines using the MOOG spectral synthesis code. He also fit the telluric-free regions of the wings of \(\text{H} \alpha\) using the Barklem et al. (2002) grid. For the same project, Luca Casagrande measured IRFM temperatures for these stars following Casagrande et al. (2010). For these five stars, we find a median offset and standard deviation for our SME values minus theirs of \(-26 \pm 29\) K for the Fe method, \(-4 \pm 22\) K for \(\text{H} \alpha\), and \(-31 \pm 73\) K for IRFM (Ramírez & Casagrande, 2013, private communication). These differences are all within the uncertainties quoted and cross-validate our adopted temperature scale. Based on our results for the field star sample, the R147 members, and the SME statistical uncertainties quoted by Valenti & Fischer (2005), we adopt the following spectroscopic parameter precisions: \(50\) K for \(T_{\text{eff}}\), \(0.06\) for \(\log g\), and \(0.04\) dex for \([\text{Fe/H}]\). Our error analysis assumes that our uncertainties are limited by the data quality and our analysis technique, and not systematics inherent in the models. As our sample is comprised of stars quite similar to the Sun, the issues that tend to plague analyses of non-solar-type stars are assumed to be largely mitigated. The procedure accurately reproduces the Sun’s properties by design, as the line data were tuned to the solar spectrum; therefore, we assume that it can safely be applied to solar twins with the same degree of accuracy, and we adopt our precision estimates as our total parameter uncertainties.

For K2-231, we found an effective temperature of \(T_{\text{eff}} = 5697\) K, surface gravity of \(\log g = 4.453\) dex, iron abundance of \([\text{Fe/H}] = +0.141\) dex, and rotational broadening of \(v \sin i = 1.95\) km s\(^{-1}\) when we adopt the macroturbulence relation from Valenti & Fischer (2005) (i.e., \(v_{\text{mac}} = 3.87\) km s\(^{-1}\)). Adopting our preferred parameters for the Dartmouth isochrone model to describe the R147 cluster (age of 3 Gyr and \([\text{Fe/H}] = +0.1\) dex) and querying the model at the spectroscopic temperature yields an isochrone-constrained surface gravity of \(\log g = 4.483\) dex, which we adopt for \(\log g\). We re-fit the spectrum with metallicity fixed to the cluster value and \(\log g\) fixed to this isochrone value, which returned \(T_{\text{eff}} = 5672\) K and \(v \sin i = 1.3\) km s\(^{-1}\), which is only 25 K cooler than the unconstrained fit.

### 3.2. Stellar mass and radius

We estimated the mass and radius of K2-231 by combining our spectroscopic results with the optical and NIR photometry provided in Table 2. We assembled photometry from Gaia (Gaia Collaboration et al. 2016a,b), the AAVSO Photometric All-Sky Survey (APASS; Henden et al. 2016) CFHT MegaCam (Hora et al. 1994) presented by Curtis et al. (2013), the Two Micron All-Sky Survey (2MASS; Skrutskie et al. 2006), the United Kingdom Infra-Red Telescope’s (UKIRT) Wide Field Infrared Camera (WFCAM; Hirst et al. 2006) that was acquired by co-author A.L. Kraus in 2011.

#### Table 2. Photometry for K2-231

| Instrument | Band | mag  | error | \(A/\Delta V\) |
|------------|------|------|-------|---------------|
| Gaia       | G    | 12.46| -     | 0.861         |
| APASS      | B    | 13.50| 0.03  | 1.297         |
| APASS      | V    | 12.71| 0.04  | 1.606         |
| CFHT MegaCam | g'  | 13.02| 0.02  | 1.167         |
| APASS      | g    | 13.07| 0.01  | 1.206         |
| CFHT MegaCam | r'  | 12.46| 0.02  | 0.860         |
| APASS      | r    | 12.47| 0.07  | 0.871         |
| CFHT MegaCam | i'  | 12.27| 0.02  | 0.656         |
| APASS      | i    | 12.26| 0.04  | 0.683         |
| 2MASS      | J    | 11.29| 0.02  | 0.291         |
| 2MASS      | H    | 11.00| 0.03  | 0.184         |
| 2MASS      | Ks   | 10.86| 0.02  | 0.115         |
| UKIRT WFCAM | J   | 11.30| 0.02  | 0.283         |
| UKIRT WFCAM | K   | 10.92| 0.02  | 0.114         |
| WISE       | W1   | 10.75| 0.02  | 0.071         |
| WISE       | W2   | 10.84| 0.02  | 0.055         |

Note—(1) Name of instrument or survey, (2) photometric band/filter employed (3,4) magnitude and uncertainty for that observation, where pipelines/surveys quoted errors below 0.01 mag, we set value to 0.02 mag for analysis, (5) interstellar reddening coefficients computed by Padova/PARSEC isochrone group (Bressan et al. 2012) for a G2V star using the Cardelli et al. (1989) extinction law and following a similar procedure to that described by Girardi et al. (2008).
and accessed from the WFCAM Science Archive.\textsuperscript{16} and NASA’s Wide-field Infrared Survey Explorer (\textit{WISE}; Wright et al. 2010).

First, we used the PARAM 1.3 input form—the “web interface for the Bayesian estimation of stellar parameters” described by da Silva et al. (2006)—to estimate the mass and radius of the host star.\textsuperscript{17} This service uses the PARSEC stellar evolution tracks (version 1.1; Bressan et al. 2012). The procedure requires as input the effective temperature, metallicity, parallax, and $V$ magnitude. We adopted the Curtis et al. (2013) distance modulus and visual extinction to estimate the de-reddened magnitude ($V_0 = V - 0.25 = 12.458$) and parallax of $\pi = 3.39$ mas yr$^{-1}$ (calculated from 295 pc).\textsuperscript{18} For parameter uncertainties, we adopt 50 K and 0.05 dex for $T_{\text{eff}}$ and $[\text{Fe}/\text{H}]$, and 0.05 mag for $V_0$ and 0.15 mas for parallax based on the uncertainty in $A_V$ and $m - M$. PARAM 1.3 returned age $t_\star = 1.7 \pm 1.6$ Gyr, mass $M_\star = 1.009 \pm 0.027 M_\odot$, log $g_\star = 4.474 \pm 0.029$ dex (cgs), and radius $R_\star = 0.934 \pm 0.029 R_\odot$.

Next, we estimated the mass and radius using the Python \texttt{isochrones} package (Morton 2015).\textsuperscript{19} We adopted the spectroscopic $T_{\text{eff}}$ and log $g$ values, the cluster metallicity and parallax, and the de-reddened broadband photometry from Table 2, and ran the fit assuming the photometry was derived from a blended and physically associated binary. Only 56\% of nearby field stars are single (Raghavan et al. 2010), so it is important to consider at least binarity when characterizing this system (Raghavan et al. also found that 11\% of nearby stars are in 3+ multiples). We used grid models from the Dartmouth Stellar Evolution Database (Dotter et al. 2008) and sampled the posteriors using MultiNest (Feroz & Hobson 2008; Feroz et al. 2009, 2013) implemented in Python with the \texttt{PyMultiNest} package (Buchner et al. 2014). Expressing uncertainties as the 68.3\% (1$\sigma$) confidence intervals of the posterior distributions, we found $M_1 = 1.013 \pm 0.016 M_\odot$, $R_1 = 0.944 \pm 0.021 R_\odot$, and $M_2 = 0.238 \pm 0.104 M_\odot$.

If the host is indeed single, then we can expect the parallax-constrained photometric analysis to return a small secondary mass with a value at approximately the threshold where its contributed flux is on par with the photometric errors (i.e., consistent with no secondary).

Based on this low secondary mass estimate, there is no evidence from the photometry for a secondary companion: the difference in magnitude between the resulting primary and secondary stars is $\Delta V = 7.29$ and $\Delta K = 4.18$, which is too large of a contrast to detect from these data (i.e., the difference between the primary and the combined magnitude of both stars is 0.001 mag in $V$ and 0.023 mag in $K$, the latter of which is on par with the measurement errors). We re-ran the fit with \texttt{isochrones} assuming a single star, which returned $M_\star = 1.004 \pm 0.017 M_\odot$, $R_\star = 0.938 \pm 0.022 R_\odot$, $d = 302 \pm 8$ pc, $A_V = 0.29 \pm 0.05$, and $t = 2.5 \pm 1$ Gyr. The age, distance, and reddening values are consistent with the CMD isochrone fitting results from Curtis et al. (2013); the mass and radius is consistent with the PARSEC/PARAM result quoted above.

To further test possible systematics in isochrone fitting methods and models we derived stellar properties using the \texttt{isoclassify} code (Huber et al. 2017),\textsuperscript{20} conditioning spectroscopic $T_{\text{eff}}$, log $g$, $[\text{Fe}/\text{H}]$, parallax, and 2MASS $JHK$ photometry on a grid of interpolated MIST isochrones (Dotter 2016). This returned $M_\star = 1.014 \pm 0.021 \pm 0.022 M_\odot$, $R_\star = 0.960 \pm 0.027 \pm 0.024 R_\odot$, $d = 309 \pm 9 - 9$ pc, $A_V = 0.09 \pm 0.27 - 0.24$ mag, and $t = 2.3 \pm 1.6 - 1.3$ Gyr, in excellent agreement with the values derived from other isochrone models and methods.

Again, systematic uncertainties in the models are likely negligible due to the Sun-like nature of the host star (whereas, for example, K dwarf models are known to diverge between PARSEC and Dartmouth; Huber et al. 2016; Curtis et al. 2013). The dispersion in masses and radii derived from the three isochrone models are well within the uncertainties returned by each method, so we adopt the maximum uncertainties from the various experiments as our final measurement uncertainties and we take the mean as our final values: $M_\star = 1.009 \pm 0.027 M_\odot$ and $R_\star = 0.945 \pm 0.027 R_\odot$.

According to the MIST model, a 3 Gyr star with mass $M_\star = 1.009 M_\odot$ and $[\text{Fe}/\text{H}] = +0.1$ dex has $T_{\text{eff}} = 5695$ K. This value is only 2 K cooler than our SME result, and so we adopt this value as the effective temperature of this star.

### 3.3. K2-231 is likely single

It is important to test K2-231 for stellar multiplicity. We need to know if it is a binary or higher-order multiple so we can confidently assume which star hosts the transiting object and how much the light from the companion(s) has diluted the observed transits.
assembled a variety of observational evidence, outlined below, that collectively indicates that K2-231 is likely single. The various constraints derived from these data are summarized in Figure 4, which shows the parameter space for a range of binary scenarios with secondaries described by $K$-band contrast (left axis) and isochrone-estimated stellar mass (right axis) as a function of projected separation in angular units (bottom axis; out to 1000 mas) and physical units (top axis; out to 300 AU).

**Photometry:** Reiterating our result from the previous subsection, modeling the broadband photometry with the isochrones package suggests that K2-231 does not have a companion with a mass $M_2 > 0.34 \, M_\odot$. Such a secondary would be at least $\sim 321$ times fainter than the primary in $V$; correcting for transit dilution would only increase the transit depth by 0.3% and the planet radius by 0.15%. Basically, the effect of any binary companion allowed by the photometric modeling is negligible. This constraint is illustrated in Figure 4 by the light blue shaded region at the top.

**Adaptive Optics Imaging and Coronagraphy:**

We acquired natural guide star AO imaging in $K'$ ($\lambda = 2.124 \, \mu m$) with NIRC2 on the Keck II telescope. We also used the “corona600” occulting spot, which has a diameter of 600 mas and an approximate transmission of 0.22% in $K'$. The observations were acquired, reduced, and analyzed following Kraus et al. (2016). Table 3 lists the $K'$ detection limits as a function of angular separation from K2-231 ranging from 150 mas to 2000 mas.

Table 4 lists six stars within 8″ that were detected, including coordinates; angular separation, position angle, and $K'$ contrast relative to K2-231; and photometry from Gaia, CFHT/MegaCam, and UKIRT/WFCAM. This table also lists four stars within 10″ detected in the UKIRT imaging that were missed by NIRC2. Figure 3 shows a 30″-square $K$-band image from UKIRT/WFCAM centered on the host star, and highlights the non-coronagraphic imaging footprint (magenta dashed-line); note that we had to offset the pointing after the first image in order to get the bright neighboring star onto the detector, which is why there is effectively a double footprint. For reference, two circles with radii of 5′′5 and 9′′ are also overlaid to show the approximate extraction apertures used to produce light curves from the $K2$ data. AO imaging and coronagraphy yielded 6 detections, 4 of which were matched in the UKIRT imaging (red circles), and two that were apparently fainter than the UKIRT source catalog limit (blue circles), but nevertheless show up in the image. Due to the placement, size, and orientation of the NIRC2 footprint, four stars within 10″ of the host were missed, but show up in WFCAM (cyan circles).

We calculated proper motions for the eight stars that matched in both Gaia and either or both MegaCam and WFCAM, and found that none but the final entry appear co-moving with R147. We also inspected optical and NIR CMDs with the cluster Dartmouth model overlaid and noted that stars 1, 3, 8, and 9 are inconsistent with membership, whereas 6, 7, and 10 appear near but beyond the base of the Dartmouth isochrone. As 6 and 7 appear to be ruled out by their discrepant proper motions, this leaves 10 as the sole candidate member in this list. Although too faint for Gaia, it is conceivable that we could measure its proper motion with additional NIRC2 images in the future: the uncertainty on $\rho$ is under 5 mas, whereas R147 moves at $\sim 28$ mas yr$^{-1}$ in declination, so two observations spaced approximately by one year should clearly reveal any co-moving stars while cancelling out the parallax effect.

Only two stars are detected within 5′′5, which is the radius of the smallest circular moving aperture that we used to extract light curves. One star is near the edge of this radius and is nearly 480 times fainter than K2-231. The other at 4′′2 southward is 40 times fainter and we consider it our primary false positive source.

These constraints are illustrated in Figure 4 by the dark blue shading, which covers the majority of the upper-right region. Masses/contrasts below the hydrogen burning limit at $\sim 0.07 \, M_\odot$ are shaded gray and found below the black horizontal line toward the bottom of the figure, which the AO limit reaches at $\sim 700$ mas—this depth is not only important for searching for stellar binaries, but also for identifying faint, unassociated stars in the background. The lowest mass star represented in the Dartmouth isochrone model is $M \approx 0.12 \, M_\odot$: we also shade this region gray and label it “VLM” for “very low mass star” to distinguish it from the region below the sub-stellar boundary while highlighting that this represents a small region of the secondary mass parameter space compared to the top-half of the figure.

**Keck/NIRC2 aperture-masking interferometry:**

We also acquired non-redundant aperture-mask interferometry data for K2-231 on 2017 June 22 in natural guide star mode, along with EPIC 219511354 for calibration. For the target and reference star, we obtained 4 (3) interferograms for a total of 80 (60) seconds on EPIC 219800881 (EPIC 219511354), which we analyzed following Kraus et al. (2008, 2011, 2016). We report no detections within the limits quoted in Table 5. These constraints are illustrated in Figure 4 by the red-shaded
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Figure 3. Image of K2-231 and neighboring stars from UKIRT/WFCAM, taken in 2011. The solid black circle shows the 9'' radius aperture used to extract the light curve. The dashed black circle has a radius of 5.5'' and is the smallest aperture we tested; the transits are still visible, which means that the object is either transiting K2-231 or the fainter star 4'' southward. The dashed magenta line traces out the Keck II NIRC2 footprint: six stars were detected, four of which cross-matched with the UKIRT catalog (red) and two that were apparently too faint though show some signal in the image (blue). Four other stars are detected in the WFCAM image within 10'', but were missed by NIRC2 due to the size, placement, and orientation of the field (cyan). Properties of these ten neighboring stars are listed in Table 4.

region, which is drawn according to the midpoints of the angular separation ranges listed in Table 5.

Spectroscopy: We observed K2-231 on 2017 June 2 (near quadrature, according to the transit ephemeris) with the High Resolution Echelle Spectrometer (HIRES; Vogt et al. 1994) on the 10 m telescope at Keck Observatory. No secondary spectral lines were found down to 1% of the brightness of the primary (~0.49 M\(_\odot\); already ruled out by photometric modeling), excluding the range of under ±10 km s\(^{-1}\) separation from the primary (Kolbl et al. 2015).

Radial Velocities—variability: We collected RVs every few years since 2007, which show no trend due to a stellar companion over the baseline of nearly ten years. These include observations with the Lick/Hamilton and MMT/Hectochelle spectrographs presented in Curtis et al. (2013), the HIRES spectrum mentioned above (Chubak et al. 2012), and the Magellan/MIKE spectra discussed earlier.\(^\text{21}\)

Separately, a team led by PI Minniti targeted R147 with the High Accuracy Radial velocity Planet Searcher (HARPS; Mayor et al. 2003) in 2013-2014 to look for exoplanets in R147 with masses greater than or approximately equal to Neptune in relatively short-period orbits and acquired six RV epochs with individual precisions of ≈10 m s\(^{-1}\).\(^\text{22}\) Data were reduced and RVs extracted with the HARPS Data Reduction Software. We downloaded the reduced data, including the pipeline RVs and uncertainties, from the ESO archive.\(^\text{23}\)

We recalculated the RVs for the Lick 2007, Hectochelle 2010, and MIKE 2016 epochs differentially relative to the solar twin member CWW 91 (NID 0739-0790842; EPIC 219698970). They were observed concurrently (Hectochelle) or close in time on the same night, with the RV zero-point of the reference star set to its median HARPS RV of 41.654 ± 0.014 km s\(^{-1}\) (5 visits over 1.9 years). For reference, Curtis et al. (2013) reported a HIRES epoch of 41.5 km s\(^{-1}\) for this reference star. CWW 91 was not observed on the same run for the MIKE 2012 epoch, so instead we calculated the zero-point with 6 other stars with HARPS RVs with concurrent MIKE observations in order to mitigate the effect of any one of those stars being an unknown binary—we note that this epoch happens to be the largest outlier, although consistent within the estimated uncertainty for our MIKE RVs.

The RVs are provided in Table 6. Averaging the two Hectochelle RVs, as well as the six HARPS RVs, yields six individual RV epochs spanning 9.8 years with an unweighted rms of 250 m s\(^{-1}\). The HARPS RV rms is 6 m s\(^{-1}\) over 10 months.

Radial Velocities—median: The median RV of 41.58 ± 0.25 km s\(^{-1}\) provides an additional stringent constraint on binarity. Consider the Hectochelle RVs: of the 50 members observed, selecting the 38 stars with RVs within 2 km s\(^{-1}\) of the cluster median, the two-night median and standard deviation RV for R147 is 41.655 ± 0.015 km s\(^{-1}\) (excluding the outlier). Barycentric velocities were calculated with the IDL code BARYCORR (Wright & Eastman 2014); see also, http://astroutils.astronomy.ohio-state.edu/exofast/barycorr.html.

Values taken from the “*ccf*G2_A.fits” files.

\(^\text{21}\) Barycentric velocities were calculated with the IDL code BARYCORR (Wright & Eastman 2014); see also, http://astroutils.astronomy.ohio-state.edu/exofast/barycorr.html.

\(^\text{22}\) ESO program 091.C-0471(A) and 095.C-0947(A); “Hunting Neptune mass planets in the nearby old, metal rich open cluster: Ruprecht 147”

\(^\text{23}\) http://archive.eso.org/wdb/wdb/adp/phase3_spectral/

\(^\text{24}\) http://archive.eso.org/wdb/wdb/adp/phase3_spectral/

\(^\text{query}\)
Table 3. Keck/NIRC2 Imaging Detection Limits

| MJD     | Filter | Number of Coronagraph Frames Exposure (s) | Total Contrast Limit ($\Delta K'$ in mag) at Projected Separation ($\rho$ in mas) |
|---------|--------|------------------------------------------|---------------------------------------------------------------------------------|
|         |        | 150 | 200 | 250 | 300 | 400 | 500 | 700 | 1000 | 1500 | 2000 |
| 57933.42| $K'$   | 6   | 120.00 | 4.9   | 6.0   | 6.4   | 6.6   | 7.3   | 7.9   | 8.6   | 8.8   | 8.9   | 8.9   |
| 57933.43| $K'$+C06 | 4   | 80.00 | ... | ... | ... | ... | 7.2 | 7.2 | 7.9 | 9.3 | 9.7 | 9.8 |

Note:—The second entry is for the coronagraphic imaging observations, which obstructs the inner 3 mas radius.

Table 4. Keck/NIRC2$^a$ and UKIRT/WFCAM Detected Neighbors

| # | RA J2000 | decl. J2000 | $\rho$ (mas) | PA (deg) | $\Delta K'$ (mag) | $G$ (mag) | $g'$ (mag) | $r'$ (mag) | $i'$ (mag) | $J$ (mag) | $K$ (mag) |
|---|----------|------------|--------------|----------|------------------|---------|---------|---------|---------|---------|---------|
| 1 | 19:16:22.005 | $-15:46:20.58$ | 4179.9 ± 1.7 | 186.488 ± 0.023 | 4.032 ± 0.003 | 16.52 | 17.12 | 16.46 | 16.24 | 15.18 | 14.76 |
| 2 | 19:16:22.319 | $-15:46:19.68$ | 5182.3 ± 2.0 | 129.033 ± 0.021 | 6.708 ± 0.017 | 18.84 | ... | ... | ... | 17.66 | 17.25 |
| 3 | 19:16:22.424 | $-15:46:13.21$ | 6429.6 ± 2.4 | 60.404 ± 0.020 | 7.243 ± 0.117 | ... | ... | ... | ... | 18.92 | 18.27 |
| 4 | 19:16:22.118 | $-15:46:23.57$ | 7388.2 ± 3.8 | 170.104 ± 0.029 | 8.521 ± 0.076 | ... | ... | ... | ... | 18.92 | 18.27 |
| 5 | 19:16:22.551 | $-15:46:16.51$ | 7693.7 ± 4.4 | 91.145 ± 0.032 | 8.216 ± 0.004 | ... | ... | ... | ... | 18.92 | 18.27 |
| 6 | 19:16:22.269 | $-15:46:23.41$ | 7759.2 ± 2.3 | 154.535 ± 0.015 | 6.677 ± 0.015 | 20.06 | 22.86 | 20.81 | 20.11 | 17.99 | 17.18 |
| 7 | 19:16:21.649 | $-15:46:13.25$ | 6585.7 | 297.421 | ... | ... | 23.48 | 21.73 | 20.71 | 18.01 | 17.21 |
| 8 | 19:16:21.807 | $-15:46:09.67$ | 7466.9 | 332.356 | ... | ... | 21.05 | 20.64 | 20.13 | 18.75 | 18.46 |
| 9 | 19:16:21.821 | $-15:46:07.48$ | 9386.6 | 339.730 | ... | ... | 18.896 | 19.07 | 18.62 | 18.32 | 17.54 | 17.06 |
| 10 | 19:16:21.439 | $-15:46:20.08$ | 9760.9 | 247.148 | ... | ... | 24.31 | 23.47 | 21.71 | 18.94 | 18.17 |

Note:—The third object was only detected in the coronagraphic observation because it fell on the edge of the NIRC2 imaging footprint; see Figure 3. The objects in the lower section were detected with UKIRT, but missed by NIRC2 due to the placement, size, and orientation of the NIRC2 field. Star #10 is the only neighbor that appears co-moving with R147 (and therefore the planet host; stars #4 and 5 were only detected in NIRC2 and so lack a second astrometric epoch needed to calculate proper motions), with a CFHT–UKIRT proper motion of ($\mu_\alpha \cos \delta, \mu_\delta$) = (3, −31) mas yr$^{-1}$, although the baseline is relatively short at ~3 years and we have not quantified the accuracy or precision with tests of anything near that faint.

$^a$The relative astrometry for the NIRC2 observations was computed with the platescale and rotation adopted from Yelda et al. (2010).

Table 5. Keck/NIRC2 aperture-masking interferometry detection limits

| Confidence | MJD | Contrast Limit ($\Delta K'$ in mag) at Projected Separation ($\rho$ in mas) |
|------------|-----|---------------------------------------------------------------------------------|
| Interval   | 10-20 | 20-40 | 40-80 | 80-160 | 160-240 | 240-320 |
| 99.9%      | 57933.4 | 0.06 | 3.02 | 4.02 | 3.79 | 3.19 | 1.96 |
| 99% only   | 57933.4 | 0.26 | 3.24 | 4.20 | 3.97 | 3.42 | 2.2  |

41.384 ± 0.70 km s$^{-1}$, which is exactly equal to the Hectochelle RV for K2-231. Even if this star is single, this equality is a coincidence given R147's intrinsic velocity dispersion. The Hectochelle RV spread is likely larger than the intrinsic cluster velocity dispersion due to some binaries lingering in the sample, and is not yet well-constrained but is currently estimated to be between $\sigma_{R147} = 0.25-0.50$ km s$^{-1}$ (see Section 3.1.2 in Curtis 2016).

Assuming $M_2 = 0.2 M_\odot$, $RV_{7} = RV_{R147},$ and $\sigma_{R147} = 0.5$ km s$^{-1}$, a hypothetical circular binary seen edge-on would require an orbital period $P_{orb} = 1175$ years ($\sim 118$ AU) for the RV semi-amplitude ($K_1$) to match the velocity dispersion. Such binaries are ruled out by the AO imaging and coronagraphy, except for phases...
where the projected separation is reduced under the detection sensitivity curve (navy blue curve in Figure 4). For shorter-period binaries, the RV of the primary will cross the cluster’s velocity at the conjunction points, but will be larger or smaller than this value during most of the orbital period, neglecting dispersion. The fact that the RV for K2-231 is exactly equal to the cluster median means that if it is a binary, we would be lucky to catch it at conjunction.

For example, consider once again the hypothetical binary described previously: $M_2 = 0.2 \, M_\odot$, $e = 0.0$, $i = 90^\circ$. If the semi-major axis is $a = 45$ AU (the approximate boundary of the AO sensitivity curve), then $P_{\text{orb}} = 146$ years and $K_1 = 1 \, \text{km s}^{-1}$. The primary only spends $0.64\%$ of its orbit within the $\sim 10 \, \text{m s}^{-1}$ uncertainty of the HARPS RV data. However, the HARPS RV precision is not the appropriate limit because we do not know the intrinsic RV (or center-of-mass velocity, $\text{RV}_\gamma$), if a binary) for this star. If $\text{RV}_\gamma \neq \langle \text{RV}_{\text{obs}} \rangle$, but instead is some other value within the cluster velocity dispersion, then it is possible that we are observing it at a quadrature point instead of conjunction, which would modestly increase the probability of randomly catching it at this orbital phase due to the longer time the star spends at the quadrature RV within the HARPS uncertainty.

### Table 6. Radial velocities for K2-231

| Date       | MJD = JD | RV     | Uncertainty | Observatory |
|------------|----------|--------|-------------|-------------|
| 2007-08-23 | 54335.789| 41.584 | 1.00        | Lick        |
| 2016-07-05 | 55382.264| 41.397 | 0.30        | Hecto       |
| 2016-07-06 | 55383.269| 41.377 | 0.30        | Hecto       |
| 2012-09-30 | 56200.644| 42.112 | 0.70        | MIKE        |
| 2013-08-10 | 56514.247| 41.580 | 0.012       | HARPS       |
| 2014-05-07 | 56784.386| 41.586 | 0.008       | HARPS       |
| 2014-05-08 | 56785.399| 41.573 | 0.007       | HARPS       |
| 2014-05-09 | 56786.404| 41.574 | 0.007       | HARPS       |
| 2014-05-27 | 56804.311| 41.570 | 0.016       | HARPS       |
| 2014-06-22 | 56830.298| 41.577 | 0.008       | HARPS       |
| 2014-07-15 | 57584.743| 41.550 | 0.70        | MIKE        |
| 2017-06-02 | 57907.075| 41.760 | 0.30        | HIRES       |

$^a$The faint neighbor referred to as “Star B” is the first object listed in Table 4 and located 4.2 degrees south of the exoplanet host at (19:16:22.319, +15:46:19.68).

**Radial Velocities—binary constraints:** These RVs, particularly the precise measurements from HARPS, are useful for constraining binary scenarios with semi-major axes closer to the primary than the region probed by adaptive optics. We estimated our detection sensitivity by generating simulated RV curves with RVLIN (Wright & Howard 2009) for binaries with semi-major axes $a < 50$ AU and secondary masses $M_2 < 0.4 \, M_\odot$ (rounding up the 0.34 $M_\odot$ limit derived from photometric modeling). We performed a simple experiment with circular orbits seen edge-on to sketch out the approximate limits on binarity in this region. For each $M_2 − a$ combination tested, we calculated the orbital period ($P_{\text{orb}}$) and the primary’s velocity semi-amplitude ($K_1$), then computed the RV time series with RVLIN. Next, we derived the optimal time of periastron passage that best aligns the observed RVs to the model, which presents a best case scenario to compute $\chi^2$. We decided that a binary was detectable if $\chi^2_{\text{binary}} > 2 \, \chi^2_{\text{single}}$, where the single-star model is a flat line running through the median RV.

The constraints derived from this simple experiment are illustrated by green shading in Figure 4. Circular, edge-on binaries with center-of-mass RVs equal to the observed median, $\text{RV}_\gamma = \langle \text{RV}_{\text{obs}} \rangle = 41.58 \, \text{km s}^{-1}$, can be ruled out for most of the remaining parameter space.

Different orbital geometries and viewing perspectives will alter the detection sensitivity. Eccentricity can increase or decrease our sensitivity depending on the specific orbital properties and the phase of the observed RVs. Inclination decreases sensitivity by reducing the RV semi-amplitude; however, it is improbable that the sensitivity would drop to zero, because it is unlikely that the binary orbital plane is exactly perpendicular to the primary–planet plane.

For now, we will conclude this discussion by stating that the evidence suggests K2-231 is likely single. Further progress can be made by simulating realistic binary systems in the cluster and testing them against the observational constraints, which is not necessary for this study. We already demonstrated that the allowed binary systems would dilute the observed transits by a negligible amount. As for which component of the hypothetical binary hosts the transits, this is accounted for when statistically validating the planet with BLENDER, discussed later in Section 4.2, by confronting the light curve with simulations of eclipsing binaries or larger planets transiting fainter stars that are physically associated, or in the background, to rule out these scenarios.

### 3.4. Activity and Rotation
et al. (1984) and Wright et al. (2004), and find tochelle spectra following procedures described in Noyes isochrones with masses greater than \( M_\odot \sim 7 \) at low mass stars and reaches down to the hydrogen burning coronagraphy (blue-lined region) probe deeper than the very mass (\( M_\odot \)).

At separations of \( \rho > 200 \) mas, the NIRC2 AO imaging and coronography (blue-lined region) probe deeper than the very low mass stars and reaches down to the hydrogen burning limit at \( \sim 700 \) mas (gray-shaded region), which is useful for searching for background blends; the NIRC2 non-redundant \( \rho > 200 \) mas, the NIRC2 AO imaging and coronography (blue-lined region) probe deeper than the very low mass stars and reaches down to the hydrogen burning limit at \( \sim 700 \) mas (gray-shaded region), which is useful for searching for background blends; the NIRC2 non-redundant masking data reach closer to the primary star, but not quite as deep (red-shaded region). Modeling the broadband photometry with isochrones rules out secondaries of any separation with masses greater than \( M_2 \gtrsim 0.34 M_\odot \) (light-blue shaded region). Combining these various constraints leaves a small region of parameter space under 45 AU (projected) for systems with \( M_2 \gtrsim 0.34 M_\odot \). The precise HARPS RVs can rule out much of this remaining parameter space for edge-on orbits (green-shaded region); accounting for possible inclination of the binary orbital plane relative to the primary–planet orbit will restrict this to smaller separations.

We measured chromospheric Ca II H & K emission indices, \( S \) and \( \log R'_{\text{HK}} \), from our MIKE and Hectochelle spectra following procedures described in Noyes et al. (1984) and Wright et al. (2004), and find \( S = 0.208 \pm 0.005 \) and \( \log R'_{\text{HK}} = -4.80 \pm 0.03 \). Figure 5 shows the Hectochelle Ca II K spectrum for K2-231, along with solar spectra taken between 2006 and the present, which are shaded red to represent the range of the contemporary solar cycle. The solar spectra were obtained by the National Solar Observatory’s Synoptic Optical Long-term Investigations of the Sun (SOLIS) facility with the Integrated Sunlight Spectrometer (ISS) on Kitt Peak (Keller et al. 2003). The observed chromospheric activity level of K2-231 is somewhat higher than the modern solar maximum (the average maximum over cycles 15–24 is \( \log R'_{\text{HK}} = -4.905 \) dex; Egeland et al. 2017), which is expected because it is \(~1.5\) Gyr younger than the Sun. Applying the activity–rotation–age relation from Mamajek & Hillenbrand (2008), a value of \( \log R'_{\text{HK}} = -4.80 \) corresponds to an age of 3.2 Gyr.

An analysis of the Ca II H & K activity for the full cluster sample is underway, and these numbers can be considered preliminary until that study is complete. However, the solar twin status of this star simplifies the calibration as we can tie it directly to solar observations. We tested this by differentially measuring \( S \) for K2-231 relative to the the SOLIS/ISS spectra and applying the conversion from their 1 A K-index to \( S \) using the Egeland et al. (2017) relations. This procedure yielded \( S = 0.2085 \), which translates to an approximate increase in \( \log R'_{\text{HK}} \) over our Hectochelle calibration of only 0.003 dex. The uncertainties are assessed by considering the observed scatter for stars with multiple observations and stars with overlapping spectra between MIKE and Hectochelle (neglecting astrophysical variability), and uncertainty in the adopted \( B - V \) when transforming \( S \) to \( \log R'_{\text{HK}} \).

\footnote{http://solis.nso.edu/iss}
The rotation period inferred as part of the activity–rotation–age procedure (i.e., from the activity–Rossby relation combined with the convective turnover time; Mamajek & Hillenbrand 2008; Noyes et al. 1984) is \( P_{\text{rot}} = 21.4 \) days. While spot modulation is clearly evident in the light curve shown in the top panel of Figure 1, a \( \sim 21 \) day signal is not immediately obvious. The apparent periodicity is closer to 6–7 days; this cannot be the true rotation period because the star would correspondingly be much more active, with \( \log R'_{\text{HK}} \sim -4.41 \) (Mamajek & Hillenbrand 2008). If there were two major spot complexes on opposite sides of the primary star, that would make the period of the modulation be half of the rotation period. If the rotational period was actually 12–14 days, we would expect \( \log R'_{\text{HK}} = -4.55 \pm 0.05 \) dex, which is still too active compared to the observed chromospheric emission.

The EVEREST light curve was produced with a stationary aperture that encompassed many bright, neighboring stars. However, those same rotation signatures are present in our 9\arcsec moving aperture light curve (not shown, but the reader can verify this with the light curve provided), which means the modulation could instead be attributed to one of the neighbors in that aperture listed in Table 4. We therefore do not report a rotation period at this time. This illustrates one of the main challenges to measuring accurate rotation periods in middle-aged clusters in crowded fields.

4. PLANET VALIDATION

First, we inspected the six individual transits for variations in depth, timing, and duration between the odd and even events that would indicate eccentricity or dissimilar stellar companions under the assumption that these are stellar eclipsing binary transits. Figure 6 shows each transit event separately, along with the EXOFAST transit model, and they are all consistent with the model and each other.

One might think that the cluster environment would create a crowded field that would complicate the photometric analysis. In fact, R147 is relatively sparse due both to the low number of (confirmed) members (\( N \approx 150 \)) and closer distance compared to clusters like NGC 6811 (295 pc versus \( \sim 1100 \) pc). However, R147’s location in the Galactic plane near Sagittarius (\( l = 21^\circ, b = -13^\circ \)) means that there are quite a few background stars. We opted for a circular moving aperture to track K2-231’s motion across its individual aperture, while excluding as many of the background stars shown in Figure 3 as possible. The aperture used to produce the EVEREST light curve that we used to identify the transiting planet contained all the bright stars shown to the south west of K2-231. Our 9\arcsec circular aperture excludes all but one of these brighter stars. We also created apertures as small as 5.5\arcsec (1.39 pixels) to reject many of the fainter stars, and the transit depth appears the same as in the larger apertures, meaning that we can attribute the transit to either of the two stars circled with the dashed line in the image.

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\( R'_{\text{HK}} \) depends on the rotation period and also the adopted \((B - V)\). The de-reddened APASS value is \((B - V)_0 = 0.72\); applying the adopted effective temperature to the table of stellar data from Pecaut & Mamajek (2013) yields \((B - V) = 0.67\). The uncertainty in each input parameter contributes a similar level of uncertainty.

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\( ^{26} \) The conversion from rotation period to \( \log R'_{\text{HK}} \) depends on the rotation period and also the adopted \((B - V)\). The de-reddened APASS value is \((B - V)_0 = 0.72\); applying the adopted effective temperature to the table of stellar data from Pecaut & Mamajek (2013) yields \((B - V) = 0.67\). The uncertainty in each input parameter contributes a similar level of uncertainty.
4.1. Star B: the bright neighbor

The star that remains blended is located approximately 4.2 south of K2-231, and we refer to this star as “star B.” The mean difference in the various photometric bands shows it to be 3.98 mag fainter than K2-231 (neglecting differences in interstellar reddening). The Gaia and CFHT/MegaCam epochs are separated by ~6.5 years, which is enough to calculate proper motions to test for association with R147, given the cluster’s relatively large proper motion in declination of $\mu_\delta = -28$ mas yr$^{-1}$. For K2-231, we measure $\mu_\delta = -25.6$ mas yr$^{-1}$, and for star B we find $\mu_\delta = -9.4$ mas yr$^{-1}$, which does not support cluster membership.

We can also model the CFHT and UKIRT photometry with isochrones under the assumption that it is a single dwarf star by applying a Gaussian prior on log $g = 4.4 \pm 0.5$, and we find a mass $M = 1.06 \pm 0.10 + 0.13$ $M_\odot$, radius $R = 1.013 - 0.16 + 0.19$ $R_\odot$, distance $d = 2204 - 343 + 406$ pc, and visual extinction $A_V = 0.63 \pm 0.18$ mag.

The 3D Galactic dust map produced from 2MASS and Pan-STARRS 1 (Green et al. 2015)\(^{27}\) toward K2-231 quotes an interstellar reddening at 300 pc (the approximate distance to R147) of $E(B-V) = 0.07 \pm 0.03 - 0.04$ (i.e., $A_V = 0.22 \pm 0.09 - 0.12$, which is consistent with the value we find from CMD isochrone fitting). According to this map, interstellar reddening is $E(B-V) = 0.16 \pm 0.02$ or $A_V = 0.50 \pm 0.06$ at 2.2 kpc, the distance we infer for Star B, and reaches a maximum value of $E(B-V) = 0.17 \pm 0.02$ at 2.28 kpc ($A_V = 0.53$).\(^{28}\) This value is consistent with our result from isochrones due to the large uncertainty, which is compounded when considering our assumption of singularity and a dwarf luminosity class. The Schlegel et al. (1998) dust map value is marginally less at $E(B-V) = 0.146$ or $A_V = 0.45$, and the re-calibrated map from Schlafly & Finkbeiner (2011) quotes $E(B-V) = 0.125$ or $A_V = 0.39$.

The proper motions and stellar properties are inconsistent with membership, meaning that Star B is likely a background star. A quick test with BLENDER (described in the next section; Torres et al. 2011a) indicates that the broad features of the transit light curve can indeed be fit reasonably well if star B is a background eclipsing binary (EB). Assuming that both the target and star B are solar-mass stars, we find a decent fit for a companion to star B of about 0.26 $M_\odot$. This EB produces a secondary eclipse, but it is very shallow (~30 ppm) and

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\(^{27}\) http://argonaut.skymaps.info/query

\(^{28}\) Using the 2015 version gives color excesses of 0.05 for R147, 0.18 for star B, and a maximum of 0.20 at 2.44 kpc.

is probably not detectable in the data, given the typical scatter of ~120 ppm. If we resolved star B, we expect that the undiluted transit due to this hypothetical EB would be ~2.5%, which could be detected from ground-based photometric observations in and out of transit. We attempted to conduct such observations with the Las Cumbres Observatory, but were unable to acquire the relevant data.

Assuming a circular orbit, the RV semi-amplitude of such a hypothetical single-lined EB is 19.8 km s$^{-1}$, which is also feasible to test and rule out with a few RV observations. We acquired two RV epochs of star B with HIRES, which were taken 7.37 and 9.93 days from mid-transit (propagated forward according to the transit ephemeris in Table 1), near the secondary eclipse and second quadrature points at phases of 0.53 and 0.72, respectively. The RVs, listed at the bottom of Table 6, are constant to within their 0.2 km s$^{-1}$ uncertainties. Furthermore, these HIRES spectra have sufficient quality to rule out secondary spectral lines down to 1% the brightness of the primary, excluding ±10 km s$^{-1}$ separation (Kolbl et al. 2015). This rules out the false positive scenario where star B is a background EB.

4.2. False alarm probability

Having excluded the only visible neighboring star within the aperture as the source of the transit signal, we then examined the likelihood of a false positive caused by unseen stars. For this we applied the BLENDER statistical validation technique (Torres et al. 2004, 2011b, 2015) that has been used previously to validate candidates from the Kepler mission (see, e.g., Torres et al. 2017; Fressin et al. 2012; Borucki et al. 2013; Barclay et al. 2013; Meibom et al. 2013; Kipping et al. 2014, 2016; Jenkins et al. 2015). For full details of the methodology and additional examples of its application we refer the reader to the first three sources above. Briefly, BLENDER models the light curve as a blend between the assumed host star and another object falling within the photometric aperture that may be an eclipsing binary or a star transited by a larger planet, such that the eclipse depths from these sources would be diluted by the brighter target to the point where they mimic shallow planetary transits. These contaminants may be either in the background or foreground of the target, or physically associated with it. Fits to the K2 light curves of a large number of such simulated blend models with a broad range of properties allows us to rule many of them out that result in poor fits, and Monte Carlo simulations conditioned on constraints from the follow-up observations (high-resolution spectroscopy, imaging, radial velocities, color information) yield a probability of
99.86% that the candidate is a planet, as opposed to a false positive of one kind or another. Thus, we consider K2-231 b to be statistically validated as a planet.

5. DISCUSSION

We have demonstrated that K2-231 is a single, solar twin member of the 3 Gyr open cluster Ruprecht 147 and that it hosts a statistically validated sub-Neptune exoplanet in a 13.84 day orbit.

5.1. Expected yield

This is the only planetary system found (as of this writing) out of 126 RV-confirmed members of R147 that were observed with K2 during Campaign 7. Neglecting the red giants (8 stars), blue stragglers (5 stars), and tight binaries (10+ stars), we searched ~100 FGK dwarfs. According to Table 4 in Fressin et al. (2013), the percentage of stars with at least one planet with an orbital period under 29 days is 0.93% for giant planets (6–22 R⊕), 0.80% for large Neptunes (4–6 R⊕), 10.24% for small Neptunes (2–4 R⊕), 12.54% for super Earths (1.25–2 R⊕), and 9.83% for Earth-sized planets (0.8–1.25 R⊕). If we assume a circular orbit, the transit probability is defined as the ratio of the sum of planetary and stellar radii to the semimajor axis, \( P_{\text{trans}} \equiv \frac{R_p + R_*}{a} \simeq (R_p/a) \). For simplicity, we assume all stars are the size of the Sun (not too unrealistic). Fressin et al. (2013) quotes the occurrence rates in eleven period ranges: we focus on 0.8–2.0, 2.0–3.2, 3.2–5.9, 5.9–10, 10–17, and 17–29 days; restricting the orbital periods to < 30 days ensures that at least two transits would be present in our ~81 day light curves. We calculate transit probabilities for the mean period for each period bin and convert these periods to semimajor axes. For (Curtis et al. 2013) and include detailed stellar properties and multiplicity informed by AO imaging, RV monitoring, and photometric modeling for our expanded RV-vetted membership list (Curtis 2016). Following the completion of the membership census, we will be able to apply our stellar properties derived from our vast photometric and spectroscopic database to the transit probability calculations and incorporate all members with light curves into our occurrence analysis. Therefore, we opt to postpone a more detailed calculation of the exoplanet occurrence rate in R147 until these two critical ingredients, membership and sensitivity, have been adequately addressed.

5.2. Comparison to field stars

Fulton et al. (2017) showed that the distribution of planetary radii is bimodal, with a valley at about 1.8 R⊕ and a peak at the larger side at 2.4 R⊕, representing sub-Neptunes, which they argue are a different class of planets than the super-Earths found on the smaller side of the gap (see their Figure 7). With a radius of ~2.5 R⊕, K2-231 b falls on the larger side of the planet radius gap (see also Rogers 2015; Weiss & Marcy 2014). Our Figure 7 presents a modified version of the bottom panel of Figure 8 from Fulton et al. (2017), which shows the completeness-corrected, two-dimensional distribution of planet size and orbital period derived from the Kepler sample—our figure compares this distribution to the

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29 In fact, Fressin et al. (2013) quotes the occurrence rates for each period range starting at 0.8 days, so we subtract the previous bin’s value from the one under consideration. For example, the occurrence rate for the 17–29 day bin is the value for the 0.8–29 day bin minus the value for 0.8–17 day bin.

Neptunes, 0.66 super Earths, and we would miss 0.57 Earths as we assume that our survey is not sensitive to the Earth-sized planets (Howell et al. 2014). Basically, in this RV-vetted sample, we expect our survey to yield ~1 planet, which we apparently found. As K2-231 b was serendipitously discovered by eye while browsing light curves in the course of a stellar rotation period search, and not by a pipeline designed to flag planetary candidates, we cannot rigorously quantify our detection sensitivity at this time (e.g., Rizzuto et al. 2016); this is especially important for the Earth and super-Earth classes because these smaller planets might not be so obviously identified visually. Furthermore, the R147 membership census is incomplete. For the “K2 Survey of Ruprecht 147,” we allocated apertures based on photometric criteria and soft proper motion cuts to strive for completeness and ensure any actual member that is eventually identified and located in the Campaign 7 field will have a K2 light curve. We selected 1176 stars that passed our tests; however, some of these targets are certainly interlopers. The impending second Gaia data release (DR2) will clarify the membership statuses of the majority of these stars. In the meantime, we are working on a new membership catalog that will supersede Curtis et al. (2013) and include detailed stellar properties and multiplicity informed by AO imaging, RV monitoring, and photometric modeling for our expanded RV-vetted membership list (Curtis 2016). Following the completion of the membership census, we will be able to apply our stellar properties derived from our vast photometric and spectroscopic database to the transit probability calculations and incorporate all members with light curves into our occurrence analysis. Therefore, we opt to postpone a more detailed calculation of the exoplanet occurrence rate in R147 until these two critical ingredients, membership and sensitivity, have been adequately addressed.
properties of K2-231 b and shows that it is found near a relative maximum. In other words, K2-231 b appears to have a fairly typical radius for a short-period (P < 29 d) planet.

5.3. Comparison to the NGC 6811 planets

Meibom et al. (2013) concluded that the frequency of planets discovered in the 1 Gyr Kepler cluster NGC 6811 is approximately equal to the Fressin et al. (2013) field rates based on two planets found out of 377 members surveyed. This is about half of the raw rate found in R147 (i.e., 1 in 100 versus 2 in 377); in other words, the same order of magnitude.

The two planets found in NGC 6811 are quite similar to K2-231 b: they are sub-Neptunes with radii of 2.8 and 2.94 R⊕ and periods of 17.8 and 15.7 days (Kepler-66 b and 67 b, respectively). This is unlikely a mere coincidence, but as Figure 7 illustrates, planets with these approximate properties are relatively more prevalent. However, that figure shows the relative occurrence of the sub-Neptunes continues, and even increases, to longer orbital periods. While the duration of the K2 survey of R147 was not long enough to identify planets in the 40–100 day regime, presumably, such planets could have been found in NGC 6811 during the Kepler prime mission. With this limited sample, it is unclear if any meaning should be drawn from this regarding possible planetary architectures that can form and survive in a dense cluster, but it is at the very least an intriguing option to consider; however, we think this is probably due to the relatively lower S/N light curves due to NGC 6811’s large distance modulus, and the reduction in transit depth and probability with increasing orbital period.

5.4. Similar planets and estimating the mass

Considering the planets with measured masses and radii in the field, there are currently five listed on exoplanets.org with 2.4 < Rp/R⊕ < 2.7, K > 1 m s⁻¹, and P > 5 day: Kepler’s 96 b, 106 c and e, 131 b, and HIP 116454 b. The basic transit and physical properties of K2-231 b and its host are similar to that of Kepler 106 c: M* = 1.0 M⊙, [Fe/H] = −0.12 dex, T eff = 5860 K, log g = 4.41 dex, V = 13, P orb = 13 days, Rp = 2.5 R⊕, and a = 0.111 AU. Importantly, the RV semi-amplitude for Kepler 106 c is K = 2.71 m s⁻¹, the planet mass is Mp = 10.4 M⊕/Marcy et al. (2014), and this mass was measured with RV observations made with Keck/HIRES.

Applying the Wolfgang et al. (2016) mass–radius relation for sub-Neptune transiting planets (i.e., Rp < 4 R⊕), where M/M⊕ = 2.7(R/R⊕)⁻¹, predicts a mass for K2-231 b of Mp = 8.75 ± 0.9 ± 1.9 M⊕, where the uncertainties represent the standard deviation of masses computed from a normally-distributed sample of radii Rp = 2.5 ± 0.2 R⊕ and the normally-distributed dispersion in mass of the relation, respectively. The Chen & Kipping (2017) probabilistic mass–radius relation, implemented with the Forecaster Python code, yields Mp = 7.2 +5.1−3.1 M⊕. Assuming a circular orbit, Kepler’s Law predicts a radial velocity semi-amplitude for K2-231 of K ≈ 2 ± 1 m s⁻¹ in this mass range. Querying the CPS chromospheric activity catalog (Isaacson & Fischer 2010) for dwarfs with similar color and activity (i.e., 0.65 < (B − V) < 0.72, −4.83 < log Rʹ HK < −4.77, and height above the main-sequence δMV < 1 mag), returns 15 stars with measured RV jitters ranging between 2.6–3.6 m s⁻¹. This might be measurable with existing precise RV instruments like HIRES or HARPS, as we know the orbit ephemeris and can strategically plan repeated observations at quadrature points to mitigate the expected jitter. K2-231 b would then become the first planet with a measured mass and density in an open cluster.

Footnote: http://exoplanets.org/detail/Kepler-106_c
APPENDIX

A. PLANETS DISCOVERED IN OPEN CLUSTERS

Table A1 lists the 24 planets that have been discovered to date in open clusters. We list KIC or EPIC IDs when available, whether the planet was discovered via transit or RV techniques (no cluster exoplanet has yet been characterized with both techniques), the \( V \) magnitude and type of host, the orbital period, planetary radius or mass (\( m \sin i \)), citations, and additional notes (e.g., “HJ,” referring to hot Jupiter). We assembled this list to determine how many planets are currently known in clusters, then decided that it might be of use and interest to the reader and so we provide it here. After we submitted this manuscript, David et al. (2018) presented a list of “known and proposed exoplanets in sub-Gyr populations detected via the transit or radial velocity method.” Their Table 1 overlaps considerably with our table due to the known cluster planets mostly being found in Hyades and Praesepe. By construction, their list does not include the NGC 6811 or M67 planets (and the R147 planet since we are announcing it now), and we do not list planets found in young associations.

A. Vanderburg produced the light curve used in this work and corroborated the initial discovery; he is supported by the NASA Sagan Fellowship. G. Torres performed the BLENDER false alarm analysis, and acknowledges partial support for this work from NASA grant NNX14AB83G (Kepler Participating Scientist Program). A.W. Howard led the acquisition of HIRES spectra of the planet host and the faint neighbor. H. Isaacson measured stellar RVs for those targets and checked the spectra for secondary light. D. Huber provided access to Keck HIRES needed to acquire those spectra and also performed the isoclassify analysis; he acknowledges support by the National Aeronautics and Space Administration under Grant NNX14AB92G issued through the Kepler Participating Scientist Program. A.L. Kraus, A.C. Rizzuto, and A.W. Mann acquired and analyzed the Keck adaptive optics data. A.W. Mann fit the light curve to measure the transit properties and contributed Figure 2. A.L. Kraus obtained the UKIRT WFCAM imaging. B.J. Fulton contributed Figure 7. C. Henze ran the BLENDER jobs on the Pleiades supercomputer and pre-processed the output. J.T. Wright advised the Ph.D. dissertation work of J.L. Curtis, which amassed much of the basic data presented herein (e.g., proprietary photometry and spectroscopy), and is the submitting and administrative PI of the K2 program GO 7035.

The remainder of the work was completed by J.L. Curtis, including the planet discovery, host star characterization, preliminary transit fitting, and synthesis of the data and contributions provided by the co-authors. He successfully led a petition for Campaign 7 to point at Ruprecht 147 and, as science PI of GO 7035, was awarded the program to survey the cluster while a graduate student at Penn State University and member of the Center for Exoplanets and Habitable Worlds. He was granted access to Magellan while serving as a SAO predoctoral fellow at the Harvard–Smithsonian Center for Astrophysics. The planet discovery and characterization work was performed after joining Columbia University.

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### Table A1. Planets in Clusters

| Planet | KIC/EPIC | Discovery | V Period | Radius / Host Notes | Citations |
|--------|----------|-----------|----------|----------------------|-----------|
| ID ID | Method (mag) | (day) | M sin i Info. | None found | 6 |
| **Pleiades (130 Myr):** | | | | | |
| ... | C4 | ... | ... | ... | None found | 6 |
| **Hyades (650 Myr):** | | | | | |
| e Tau b | 210754593 | RV | 3.53 | 594.9 | 7.6 M_{Jup} | Giant | 1st ever | 19 |
| HD 285507 b | 210495452 | RV | 10.47 | 6.09 | 0.97 M_{Jup} | M4.5 | | 18 |
| K2-25 b | 210490365 | Tr | 15.88 | 4.385 | 3.43 M_{⊙} | M4.5 | | 5, 10 |
| K2-136-A b | 247589423 | Tr | 11.20 | 7.98 | 0.99 R_{⊕} | K5.5 | Stellar binary | 4, 12 |
| K2-136-A c | 247589423 | Tr | 11.20 | 17.31 | 2.91 R_{⊕} | K5.5 | Stellar binary | 4, 12 |
| K2-136-A d | 247589423 | Tr | 11.20 | 25.58 | 1.45 R_{⊕} | K5.5 | Stellar binary | 4, 12 |
| **Praesepe (650 Myr):** | | | | | |
| Pr0201 b | 211998346 | RV | 10.52 | 4.43 | 0.54 M_{Jup} | late-F HJ, “two b’s” | 17 |
| Pr0211 b | 211936827 | RV | 12.15 | 2.15 | 1.844 M_{Jup} | late-G HJ, “two b’s” | 17 |
| Pr0211 c | 211936827 | RV | 12.15 | >3500 | 7.9 M_{Jup} | late-G | Eccentric; 1st multi | 9 |
| K2-95 b | 211916756 | Tr | 17.27 | 10.14 | 3.7 R_{⊕} | | | 7, 11, 14, 15 |
| K2-100 b | 211908866 | Tr | 10.373 | 1.67 | 3.5 R_{⊕} | 1.18 M_{⊕} | | 1, 7, 11, 16 |
| K2-101 b | 21193977 | Tr | 12.552 | 14.68 | 2.0 R_{⊕} | 0.80 M_{⊕} | | 1, 7, 11, 16 |
| K2-102 b | 211970147 | Tr | 12.758 | 9.92 | 1.3 R_{⊕} | 0.77 M_{⊕} | | 11 |
| K2-103 b | 211822797 | Tr | 14.661 | 21.17 | 2.2 R_{⊕} | 0.61 M_{⊕} | | 11 |
| K2-104 b | 211969807 | Tr | 15.770 | 1.97 | 1.9 R_{⊕} | 0.51 M_{⊕} | | 7, 11 |
| EPIC 211901114 b | 211901114 | Tr | 16.485 | 1.65 | 9.6 R_{⊕} | 0.46 M_{⊕} | Candidate | 11 |
| **NGC 2423 (740 Myr):** | | | | | |
| TYC 5409-2156-1 b | .. | RV | 9.45 | 714.3 | 10.6 M_{Jup} | Giant | | 8 |
| **NGC 6811 (1 Gyr):** | | | | | |
| Kepler-66 b | 9836149 | Tr | 15.3 | 17.82 | 2.80 R_{⊕} | 1.04 M_{⊕} | | 13 |
| Kepler-67 b | 9532052 | Tr | 16.4 | 15.73 | 2.94 R_{⊕} | 0.87 M_{⊕} | | 13 |
| **Ruprecht 147 (3 Gyr):** | | | | | |
| K2-231 b | 219890881 | Tr | 12.71 | 13.84 | 2.5 R_{⊕} | solar twin | | This work |
| **M67 (4 Gyr):** | | | | | |
| YBP 401 b | .. | RV | 13.70 | 4.087 | 0.42 M_{Jup} | F9V HJ | | 2, 3 |
| YBP 1194 b | 211411531 | RV | 14.68 | 6.960 | 0.33 M_{Jup} | G5V | HJ | 2, 3 |
| YBP 1514 b | 211416296 | RV | 14.77 | 5.118 | 0.40 M_{Jup} | G5V | HJ | 2, 3 |
| SAND 364 b | 211403356 | RV | 9.80 | 121 | 1.57 M_{Jup} | K3III | | 2, 3 |
| SAND 978 b^{d} | .. | RV | 9.71 | 511 | 2.18 M_{Jup} | K4II | Candidate | 2, 3 |

**References**

(1) Barros et al. (2016); (2) Brucalassi et al. (2014); (3) Brucalassi et al. (2017); (4) Ciardi et al. (2017); (5) David et al. (2016a); (6) Gaidos et al. (2017); (7) Libralato et al. (2016); (8) Lovis & Mayor (2007); (9) Malavolta et al. (2016); (10) Mann et al. (2016a); (11) Mann et al. (2017a); (12) Mann et al. (2017b); (13) Meibom et al. (2013); (14) Obermeier et al. (2016); (15) Pepper et al. (2017); (16) Pope et al. (2016); (17) Quinn et al. (2012); (18) Quinn et al. (2014); (19) Sato et al. (2007)

^{a} See also, Mann et al. (2017a), Pepper et al. (2017)

^{b} Lovis & Mayor (2007) also announced a sub-stellar object in NGC 4349, but it has a minimum mass of 19.8 M_{Jup}, greater than the planet–brown dwarf boundary at 11.4-14.4 M_{Jup}, and so we do not included it here.

^{c} Nardiello et al. (2016) announced some candidates, which they concluded are likely not members of M67.

^{d} Brucalassi et al. (2017) refer to this detection as a planet candidate and state that YBP 778 and YBP 2018 are also promising candidates.
non-HST data is provided by the NASA Office of Space Science via grant NNX09AF08G and by other grants and contracts.

This research has made use of the Periodogram Service of the NASA Exoplanet Archive, which is operated by the California Institute of Technology, under contract with the National Aeronautics and Space Administration under the Exoplanet Exploration Program.

This research has made use of the Exoplanet Orbit Database and the Exoplanet Data Explorer at exoplanets.org (Han et al. 2014).

This work is based on observations obtained with MegaCam, a joint project of CFHT and CEA/DAPNIA, at the CanadaFrance-Hawaii Telescope (CFHT), which is operated by the National Research Council (NRC) of Canada, the Institute National des Sciences de l’Univers of the Centre National de la Recherche Scientifique of France, and the University of Hawaii. Observing time was granted by the University of Hawaii Institute for Astronomy TAC. These data were reduced at the TERAPIX data center located at the Institut d’Astrophysique de Paris.

This publication makes use of data products from the Two Micron All Sky Survey, which is a joint project of the University of Massachusetts and the Infrared Processing and Analysis Center/California Institute of Technology, funded by NASA and the NSF.

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Software: BARYCORR (Wright & Eastman 2014), batman (Kreidberg 2015), EXOFAST (Eastman et al. 2013), forecaster (Chen & Kipping 2017), isoclassify (Huber et al. 2017), RVLIN (Wright & Howard 2009), SME (Valenti & Piskunov 1996)

REFERENCES

Adams, F. C. 2010, ARA&A, 48, 47
Adams, F. C., Proszkow, E. M., Fatuzzo, M., & Myers, P. C. 2006, ApJ, 641, 504

31 https://www.cosmos.esa.int/web/gaia/dpac/consortium

Altmann, M., Roeser, S., Demleitner, M., Bastian, U., & Schilbach, E. 2017, A&A, 600, L4
Barclay, T., Burke, C. J., Howell, S. B., et al. 2013, ApJ, 768, 101
Barklem, P. S., Stempels, H. C., Allende Prieto, C., et al. 2002, A&A, 385, 951
Barros, S. C. C., Demangeon, O., & Deleuil, M. 2016, A&A, 594, A100
Bernstein, R., Shectman, S. A., Gunnels, S. M., Mochnacki, S., & Athey, A. E. 2003, in Proc. SPIE, Vol. 4841, Instrument Design and Performance for Optical/Infrared Ground-based Telescopes, ed. M. Iye & A. F. M.
Moorwood, 1694
Bonelli, I. A., Smith, K. W., Davies, M. B., & Horne, K. 2001, MNRAS, 322, 859
Bonnell, I. A., Smith, K. W., Davies, M. B., & Horne, K. 2001, MNRAS, 322, 859
Borucki, W. J., Agol, E., Fressin, F., et al. 2013, Science, 340, 587
Bressan, A., Marigo, P., Girardi, L., et al. 2012, ArXiv e-prints, arXiv:1208.4498
Brewer, J. M., Fischer, D. A., Basu, S., Valenti, J. A., & Piskunov, N. 2015, ApJ, 805, 126
Brewer, J. M., Fischer, D. A., Valenti, J. A., & Piskunov, N. 2016, ArXiv e-prints, arXiv:1606.07929
Brucalassi, A., Pasquini, L., Saglia, R., et al. 2014, A&A, 561, L9
—. 2016, ArXiv e-prints, arXiv:1606.05247
Brucalassi, A., Koppenhoefer, J., Saglia, R., et al. 2017, A&A, 603, A85
Buchner, J., Georgakakis, A., Nandra, K., et al. 2014, A&A, 564, A125
Cai, M. X., Kouwenhoven, M. B. N., Portegies Zwart, S. F., & Spurzem, R. 2017, ArXiv e-prints, arXiv:1706.03789
Cardelli, J. A., Clayton, G. C., & Mathis, J. S. 1989, ApJ, 345, 245
Casagrande, L., Ramírez, I., Meléndez, J., Bessell, M., & Asplund, M. 2010, A&A, 512, A54
Chen, J., & Kipping, D. 2017, ApJ, 834, 17
Chubak, C., Marcy, G., Fischer, D. A., et al. 2012, ArXiv e-prints, arXiv:1207.6212
Ciardi, D. R., Crossfield, I. J. M., Feinstein, A. D., et al. 2017, ArXiv e-prints, arXiv:1709.10398
Claret, A., & Bloemen, S. 2011, A&A, 529, A75
Curtis, J., Vanderburg, A., Montet, B., et al. 2016, A warm brown dwarf transiting a solar analog in a benchmark cluster, , , doi:10.5281/zenodo.58758.
http://dx.doi.org/10.5281/zenodo.58758
Curtis, J. L. 2016, PhD thesis, Penn State University
—. 2017, AJ, 153, 275
Curtis, J. L., Wolfgang, A., Wright, J. T., Brewer, J. M., & Johnson, J. A. 2013, AJ, 145, 134
da Silva, L., Girardi, L., Pasquini, L., et al. 2006, A&A, 458, 609
David, T. J., Conroy, K. E., Hillenbrand, L. A., et al. 2016a, AJ, 151, 112
David, T. J., Hillenbrand, L. A., Petigura, E. A., et al. 2016b, Nature, 534, 658
David, T. J., Mamajek, E. E., Vanderburg, A., et al. 2018, ArXiv e-prints, arXiv:1801.07320
de Juan Ovelar, M., Krijgsman, J. M. D., Bressert, E., et al. 2012, A&A, 546, L1
Donati, J. F., Moutou, C., Malo, L., et al. 2016, Nature, 534, 662
Donati, J.-F., Yu, L., Moutou, C., et al. 2017, MNRAS, 465, 3343
Dotter, A. 2016, ApJS, 222, 8
Dotter, A., Chaboyer, B., Jevremović, D., et al. 2008, ApJS, 178, 89
Eastman, J., Gaudi, B. S., & Agol, E. 2013, PASP, 125, 83
Egeland, R., Soon, W., Balunas, S., et al. 2017, ApJ, 835, 25
Feroz, F., & Hobson, M. P. 2008, MNRAS, 384, 449
Feros, F., Hobson, M. P., & Bridges, M. 2009, MNRAS, 398, 1601
Feroz, F., Hobson, M. P., Cameron, E., & Pettitt, A. N. 2013, ArXiv e-prints, arXiv:1306.2144
Foreman-Mackey, D., Hogg, D. W., Lang, D., & Goodman, J. 2013, PASP, 125, 306
Fregeau, J. M., Chatterjee, S., & Rasio, F. A. 2006, ApJ, 640, 1086
Fressin, F., Torres, G., Rowe, J. F., et al. 2012, Nature, 482, 195
Fressin, F., Torres, G., Charbonneau, D., et al. 2013, ApJ, 766, 81
Fulton, B. J., Petigura, E. A., Howard, A. W., et al. 2017, AJ, 154, 109
Gaia Collaboration, Prusti, T., de Bruijne, J. H. J., et al. 2016a, A&A, 595, A1
Gaia Collaboration, Brown, A. G. A., Vallenari, A., et al. 2016b, A&A, 595, A2
Gaidos, E., Mann, A. W., Rizzuto, A., et al. 2017, MNRAS, 464, 850
Geller, A. M., Latham, D. W., & Mathieu, R. D. 2015, AJ, 150, 97
Girardi, L., Dalcanton, J., Williams, B., et al. 2008, PASP, 120, 583
Green, G. M., Schlafly, E. F., Finkbeiner, D. P., et al. 2015, ApJ, 810, 25
Haisch, Jr., K. E., Lada, E. A., & Lada, C. J. 2001, ApJL, 553, L153
Han, E., Wang, S. X., Wright, J. T., et al. 2014, PASP, 126, 827
Henden, A. A., Templeton, M., Terrell, D., et al. 2016, VizieR Online Data Catalog, 2336
Henry, T. J., Ianna, P. A., Kirkpatrick, J. D., & Jahreiss, H. 1997, AJ, 114, doi:10.1086/118482

Curtis et al.
A sub-Neptune exoplanet in Ruprecht 147

Henry, T. J., Jao, W.-C., Subasavage, J. P., et al. 2006, AJ, 132, 2360

Hirst, P., Casali, M., Adamson, A., Ives, D., & Kerr, T. 2006, in Proc. SPIE, Vol. 6269, Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series, 62690Y

Hora, J. L., Luppino, G. A., & Hodapp, K.-W. 1994, in Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series, Vol. 2198, Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series, ed. D. L. Crawford & E. R. Craine, 498–503

Howell, S. B., Soebeck, C., Haas, M., et al. 2014, PASP, 126, 398

Huber, D., Bryson, S. T., Haas, M. R., et al. 2016, ApJS, 224, 2

Huber, D., Zinn, J., Bojsen-Hansen, M., et al. 2017, ApJ, 844, 102

Isaacson, H., & Fischer, D. 2010, ApJ, 725, 875

Janes, K. 1996, J. Geophys. Res., 101, 14853

Jenkins, J. M., Twicken, J. D., Batalha, N. M., et al. 2015, AJ, 150, 56

Keller, C. U., Harvey, J. W., & Giampapa, M. S. 2003, in Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series, Vol. 4853, Innovative Telescopes and Instrumentation for Solar Astrophysics, ed. S. L. Keil & S. V. Avakyan, 194–204

Kipping, D. M. 2013, MNRAS, 435, 2152

Kipping, D. M., Torres, G., Buchhave, L. A., et al. 2014, ApJ, 795, 25

Kipping, D. M., Torres, G., Henze, C., et al. 2016, ApJ, 820, 112

Kolbl, R., Marcy, G. W., Isaacson, H., & Howard, A. W. 2015, AJ, 149, 18

Kovács, G., Zucker, S., & Mazeh, T. 2002, A&A, 391, 369

Kraus, A. L., Ireland, M. J., Huber, D., Mann, A. W., & Dupuy, T. J. 2016, AJ, 152, 8

Kraus, A. L., Ireland, M. J., Martinache, F., & Hillenbrand, L. A. 2011, ApJ, 731, 8

Kraus, A. L., Ireland, M. J., Martinache, F., & Lloyd, J. P. 2008, ApJ, 679, 762

Kreidberg, L. 2015, PASP, 127, 1161

Lada, C. J., & Lada, E. A. 2003, ARA&A, 41, 57

Libralato, M., Nardiello, D., Bedin, L. R., et al. 2016, MNRAS, 463, 1780

Livingston, J. H., Dai, F., Hirano, T., et al. 2017, ArXiv e-prints, arXiv:1710.07203

Lovis, C., & Mayor, M. 2007, A&A, 472, 657

Luger, R., Agol, E., Kruse, E., et al. 2016, AJ, 152, 100

Luger, R., Kruse, E., Foreman-Mackey, D., Agol, E., & Saunders, N. 2017, ArXiv e-prints, arXiv:1702.05488

Malavolta, L., Nascimbeni, V., Piotto, G., et al. 2016, A&A, 588, A118

Malmberg, D., de Angeli, F., Davies, M. B., et al. 2007, MNRAS, 378, 1207

Mamajek, E. E., & Hillenbrand, L. A. 2008, ApJ, 687, 1264

Mamajek, E. E., Prsa, A., Torres, G., et al. 2015, ArXiv e-prints, arXiv:1510.07674

Mandel, K., & Agol, E. 2002, ApJL, 580, L171

Mann, A. W., Gaidos, E., Mace, G. N., et al. 2016a, ApJ, 818, 46

Mann, A. W., Newton, E. R., Rizzuto, A. C., et al. 2016b, AJ, 152, 61

Mann, A. W., Gaidos, E., Vanderburg, A., et al. 2017a, AJ, 153, 64

Mann, A. W., Vanderburg, A., Rizzuto, A. C., et al. 2017b, ArXiv e-prints, arXiv:1709.10328

Marcy, G. W., Isaacson, H., Howard, A. W., et al. 2014, ApJS, 210, 20

Mayor, M., & Queloz, D. 1995, Nature, 378, 355

Mayor, M., Pepe, F., Queloz, D., et al. 2003, The Messenger, 114, 20

Meibom, S., Barnes, S. A., Latham, D. W., et al. 2011, ApJL, 733, L9

Meibom, S., Torres, G., Fressin, F., et al. 2013, Nature, 499, 55

Michalik, D., Lindegren, L., & Hobbs, D. 2015, A&A, 574, A115

Morton, T. D. 2015, isochrones: Stellar model grid package, Astrophysics Source Code Library, , ascl:1503.010

Nardiello, D., Libralato, M., Bedin, L. R., et al. 2016, MNRAS, 463, 1831

Nowak, G., Palle, E., Gandolfi, D., et al. 2017, AJ, 153, 131

Noyes, R. W., Weiss, N. O., & Vaughan, A. H. 1984, ApJ, 287, 769

Obermeier, C., Henning, T., Schlieder, J. E., et al. 2016, AJ, 152, 223

Pecaut, M. J., & Mamajek, E. E. 2013, ApJS, 208, 9

Pepper, J., Gillen, E., Parviainen, H., et al. 2017, AJ, 153, 177

Pope, B. J. S., Parviainen, H., & Aigrain, S. 2016, MNRAS, 461, 3399

Prša, A., Harmanec, P., Torres, G., et al. 2016, AJ, 152, 41

Quinn, S. N., White, R. J., Latham, D. W., et al. 2012, ApJL, 756, L33

Raghavan, D., McAlister, H. A., Henry, T. J., et al. 2010, ApJS, 190, 1
