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First Germanium-Based Constraints on Sub-MeV Dark Matter with the EDELWEISS Experiment

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We present the first Ge-based constraints on sub-MeV/c² dark matter (DM) particles interacting with electrons using a 33.4 g Ge cryogenic detector with a 0.53 electron-hole pair (rms) resolution, operated underground at the Laboratoire Souterrain de Modane. Competitive constraints are set on the DM-electron scattering cross section, as well as on the kinetic mixing parameter of dark photons down to 1 eV/c². In particular, the most stringent limits are set for dark photon DM in the 6 to 9 eV/c² range. These results demonstrate the high relevance of Ge cryogenic detectors for the search of DM-induced eV-scale electron signals.

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Direct-detection experiments are progressing rapidly in the search of nuclear scattering events due to weakly interacting massive particles on the GeV/c² to TeV/c² mass scale [1–4]. However, there are compelling models that motivate us to extend direct searches to dark matter (DM) particles in the eV/c² to MeV/c² range, where the signal would be an electron recoil arising either from the absorption of a dark photon (bosonic DM) [5,6], or the elastic scattering of a dark fermion [7]. For these searches—requiring kilogram-scale detectors with ~1 eV detection thresholds to fully cover benchmark models [8]—semiconductor detectors are uniquely positioned due to their band-gap energies an order of magnitude lower than the ionization potential of xenon-based detectors [9].

Recent progress has been made with silicon-based gram-scale devices, using CCDs [10,11] and cryogenic detectors [12] now sensitive to single electron-hole pairs. Efforts are ongoing to reduce dark currents and radioactive background to the levels required for scaling up to more massive arrays. In this context, phonon-mediated germanium detectors offer an attractive alternative. The smaller band-gap energy of Ge relative to Si (Eg = 0.67 eV vs 1.11 eV [13,14]) naturally yields an increased sensitivity to lighter DM particles. In addition, the difference in composition paves the way to a better understanding of the origin of the background observed in semiconductor detectors at this new eV-scale frontier.

In phonon-mediated cryogenic detectors, the drift of N electron-hole pairs across a voltage difference ∆V produces additional phonons whose energy ENTL = NεΔV (ε is the elementary charge) adds to the initial recoil energy. This effect called Neganov-Trofimov-Luke (NTL) [15,16] essentially turns a cryogenic calorimeter (operated at ∆V = 0 V) into a charge amplifier of mean gain ⟨g⟩ = (1 + εΔV/e), where e = 3.0 eV (3.8 eV) is the mean ionization energy in Ge (Si) [17] for electron recoils.

Recently, the EDELWEISS Collaboration achieved a 17.7 eV phonon baseline resolution (rms) with a 33.4 g Ge bolometer operated above ground [18]. To reach sub-electron-hole pair resolution, a similar detector was equipped with electrodes to take advantage of the expected 1/⟨g⟩ improvement of the charge resolution with applied voltage.
In this Letter, we exploit the resulting sensitivity to energy deposits as low as the band-gap energy to set competitive constraints on sub-MeV/c^2 DM particles interacting with electrons, as well as on dark photons down to 1 eV/c^2.

The DM search was performed at the Laboratoire Souterrain de Modane (France) with a detector consisting of a 33.4 g cylindrical high-purity Ge crystal (\(20 \times 20 \text{ mm}\)). Two aluminum electrodes were lithographed on each of the two planar surfaces: a central electrode in a grid layout (square meshing with a 500 \(\mu\text{m}\) pitch), and a guard electrode made of a concentric ring on the outer edges of the surface. A 2 \(\times\) 2 mm\(^2\) area was left empty at the center of one face to allow for the direct gluing of a Ge neutron-transmutation-doped (NTD) [19] thermal phonon sensor on the crystal. The center and guard electrodes on top and bottom are biased to voltages with the same magnitude but opposite polarities \(V_{\text{top}} = -V_{\text{bot}}\). Each electrode is connected to an ionization channel that is read out independently. The data acquisition system and readout electronics are the same as in [20]. The data from the phonon and ionization channels were digitized at a frequency of 100 kHz, filtered, averaged, and continuously stored on disk with a digitization rate of 500 Hz.

The detector was maintained at a regulated temperature between 20.0 or 20.7 mK between January and October 2019. Most of that period was devoted to detector studies. The detector was exposed again to a strong \(^{60}\text{Co}\) source for 15 h, in order to reactivate it and confirm the stability of the detector response with high statistics.

The study of the detector performance and stability led to the choice of a bias of 78 V for a DM search involving electron recoils. A continuous sequence of runs at 78 V was set aside for this search. The baseline resolution derived from random trigger samples was studied hour by hour. The first three days were discarded as the baseline resolution reached its plateau within a few days after the data taking began. The remaining 89 h of data were separated into a blind sample of 58 h sandwiched between a nonblind sample of 21 h plus 9 h of data. The remaining 89 h of data were separated into a blind sample of 58 h sandwiched between a nonblind sample of 21 h plus 9 h of data. The stability of the energy scale was monitored day by day in the nonblind sample and hour by hour in the blind sample. The average baseline energy resolution in the blind sample is 1.63 eV_{\text{ee}} (0.54 electron-hole pairs), corresponding to a phonon resolution of 44 eV, once the NTL gain of 27 is considered. The average baseline resolution in the nonblind sample is 3% better (1.58 eV_{\text{ee}}, or 0.53 pairs). Three days after the data taking was discarded, the detector was exposed again to a strong \(^{60}\text{Co}\) source for 15 h, in order to reconvert it and confirm the stability of the detector response with high statistics.
The data processing is essentially the same as in [18] and uses the numerical procedure described in [24] to derive a filter that optimizes the signal-to-noise ratio over the entire frequency domain. An iterative search for pulses in the filtered data stream is performed using a decreasing energy ordering rule. After the pulse with the largest amplitude is found, the 1024 samples centered on the time position $t_0$ of the pulse are stored as an event. The corresponding time trace ($\Delta t = 2.048$ s) is excluded from the search in the next iteration, proceeding downward in amplitude. The procedure stops when there is no time interval greater than $\Delta t$ left in the stream. Thus, there is no trigger threshold set in energy and the trigger rate is driven by the choice of $\Delta t$, not by the physical event rate. The energy dependence of the dead time induced by this procedure is fully taken into account in the evaluation of the trigger efficiency using a pulse simulation described below. The pulse amplitudes are evaluated by minimizing the following $\chi^2_k$ function in the frequency domain:

$$\chi^2_k(a, t_0) = \sum_i \frac{|\hat{v}(f_i) - a \hat{s}(f_i) e^{-2\pi i f_0 t_0}|^2}{J(f_i)},$$

where $J(f_i)$ is the noise power spectral density, $\hat{v}(f_i)$ is the Fourier transform of the event time trace, and $a$ is the amplitude of the signal template $s_k$ normalized to unity. The subscript $k$ designates the so-called “normal” and “fast” categories of events, each corresponding to a different pulse template. Normal events refer to particle interactions occurring in the Ge target crystal. For this category, we use a template based on 10.37 keV event pulses which are characterized by a rise time of $\sim 7$ ms. Fast events stand out with a considerably shorter rise time ($<1$ ms), compatible with interactions occurring directly in the NTD. Their template is based on events selected from the data on the basis of their characteristic time constant and the absence of ionization signal. The data selection is based on the values of $\chi^2_{\text{normal}}$ and on the difference $\Delta \chi^2 = \chi^2_{\text{normal}} - \chi^2_{\text{fast}}$, whereas pulse amplitude estimation is based on the normal template only.

The trigger and cut efficiencies were determined using a complete signal simulation procedure [18]. Pulses of known energy are injected at random times throughout the entire real data streams at a rate of $\sim 0.02$ Hz in order not to increase the dead time by more than $\sim 1\%$. Each simulated pulse corresponds to a trace randomly chosen among a selection of $K$-line events, scaled to the desired fraction of 10.37 keV and added to the data stream. The set of preselected traces consists of 858 events recorded at 78 V after postsearch activation with energies between 1.5 and 11 keV, thus including $K$-tail events. Because of uncertainties on how to model properly low-energy events associated with incomplete NTL effect, only events whose energy before scaling is less than 470 eV ($\sim 3\sigma$) away from the 10.37 keV peak are considered as contributing to the signal efficiency. This way, we conservatively neglect the sensitivity from events with incomplete charge collection while accounting for the dead time these may induce via pileups. This results in an overall 25% efficiency loss [25]. The trigger and analysis cut efficiencies are measured as the fraction of simulated events surviving the reconstruction procedure and the selection criteria on $\chi^2_{\text{normal}}$ and $\Delta \chi^2$. After all cuts the efficiency for simulated single (double) electron-hole pair events of 3 eVee (6 eVee) is 4% (22%). More detailed information about signal efficiencies can be found in the Supplemental Material [26]. Figure 2 shows the energy spectrum of the selected events in the 58 h of DM search. The efficiency-corrected rate at 25 eVee corresponds to $1.6 \times 10^5$ events/kg/day/keV. Comparison of the total phonon energy spectra recorded at various biases indicates that most of the rate observed above 680 eV (25 eVee at 78 V and 30 eVee at 66 V) corresponds to events not affected by the NTL amplification. The origin of these so-called “heat-only” events, which are also responsible for the rise of the spectrum below 100 eVee in Fig. 1, is still under investigation [27].

However, this comparative study does not provide clear information about the nature of the events observed below 25 eVee in the DM search data. In Fig. 2, we show the contributions of $N = [1, ..., 5]$ electron-hole pair events obtained from the pulse simulation for DM models described below. For $N > 1$, the reconstructed energy spectra associated with $N$-pair events peak at $N \times 3$ eVee. However, the spectrum associated with single-pair events is biased toward higher energy as only those with
reconstructed energies above $\sim 3$ eV are selected by the trigger algorithm. The detector resolution is not sufficient to unambiguously disentangle single-pair from noise-triggered events. It is, however, able to provide an upper bound on single-pair (or N-pair events), and more generally to the DM signals discussed below.

The DM-electron scattering rate as a function of the energy transferred to the electron $E_e$ is given by [7]:

$$\frac{dR}{dE_e} \propto \tilde{\sigma}_e \int \frac{dq}{q^2} \eta(E_e, q, m_x)|F_{DM}(q)|^2 |f_c(q, E_e)|^2,$$

(2)

where $\tilde{\sigma}_e$ is a reference cross section for free electron scattering and $m_x$ is the DM particle mass. The term $\eta$ encapsulates DM halo physics and is calculated assuming a local DM density of $\rho_{DM} = 0.3$ GeV/cm$^3$, a galactic escape speed $v_{esc} = 544$ km/s and an asymptotic circular speed $v_0 = 220$ km/s [28,29]. The momentum-transfer $q$ dependence of the interaction is described by the form factor $F_{DM}$. The crystal form factor $f_c$ is related to the probability that a momentum-transfer $q$ yields an electron transition of energy $E_e$, given the details of the Ge crystal band structure. It is computed with the QEdark module [7] of the quantum ESPRESSO package [30].

For the search of a dark photon, its absorption rate per unit time and target mass is calculated according to [6]

$$R = \frac{1}{\rho} \frac{dN_{DM}}{m_{\gamma}} \kappa_{\gamma\gamma}(m_{\gamma}, \delta) \sigma_1(m_{\gamma}),$$

(3)

where $\rho$ is the target density, $m_{\gamma}$ is the dark photon mass, and the expected signal is a monoenergetic electron transition of energy $E_e = m_{\gamma} c^2$. $\kappa_{\gamma\gamma}$ is the effective mixing angle which is linearly proportional to the kinetic mixing parameter $\kappa$ between the standard model (SM) photon and its hidden counterpart, and $\sigma_1$ is the real part of the complex conductivity $\tilde{\sigma}$. In Ge, the temperature dependence of $\tilde{\sigma}$ above 1 eV is small, allowing us to use the room temperature data from [6] down to 1 eV/c$^2$.

The signal recorded in the detector, calibrated in eV$_{ee}$, is $E = (E_e + N e \Delta V)/(1 + e \Delta V/e)$, thus requiring a discrete distribution function to ascribe a probability $P(N|E_e)$ of producing $N$ electron-hole pairs following an electron transition of energy $E_e$. A variety of ionization models have been proposed [7,12,31]. Here, we use the ionization model of [12] (with $F = 0.15$) in order to facilitate the comparison of our results with those obtained with this Si phonon-mediated detector.

The method to derive DM constraints from the observed spectrum is the same as in [18]. Prior to the unblinding of the search sample, DM-mass dependent regions of interest (ROIs) were chosen such as to optimize the expected sensitivity based on a kernel density estimation of the 30 h of nonblind data. 90% C.L. Poisson upper limits were derived, considering all events in the search sample ROIs upon unblinding as DM candidates. Because no background subtraction is performed, this procedure yields conservative bounds even if a signal is present in the nonblind data set.

These limits are shown as the solid red lines in Fig. 3. The top and middle panels are the limits for the interaction cross-section $\tilde{\sigma}_e$ of DM particles with electrons via a heavy ($F_{DM} = 1$) or light mediator ($F_{DM} \propto 1/q^2$), respectively. The bottom panel shows the limits on the kinetic mixing parameter $\kappa$ of a dark photon with a SM one. Variation on the energy scale of $\pm 2\%$ would affect the limits on $\kappa$ (or $\tilde{\sigma}_e$) by less than 10% (20%). Temperature effects on $\sigma_1$ in Ge for electron signals above 1 eV$_{ee}$ are expected to be small: it was nevertheless verified that a 20% variation of $\sigma_1$ would affect the limits on $\kappa$ by at most $\pm 10\%$. The excluded event rates are at levels where Earth-shielding effects are negligible [32].

The light red band shows the effect of varying the Fano factor $F$ between 0.30 and the lower bound set by the Bernoulli distribution [31]. The dotted red lines are the limits derived using the linear ionization model described in [7], whereby the $P(N|E_e)$ distribution is replaced by a delta function at the closest integer less or equal to $N = 1 + (E_e - E_g)/e$. This results in a stepwise evolution of the limits on $\kappa$ as a function of $m_{\gamma}$, as the sensitivity for a given mass is entirely based on the limit on the rate of N-pair events. The noticeable difference around $m_{\gamma} = 3$ eV/c$^2$ between the dark photon limits obtained when considering these two different ionization models is due to the minimum energy needed to create two-pair events ($e + e + E_g$). The EDELWEISS sensitivity below $m_{\gamma} = 3$ eV/c$^2$ derives from a 90% C.L. upper bound of 4 Hz on the efficiency-corrected rate of single-pair events in the detector. The upper limit on the two-pair event rate is 0.08 Hz. The single-electron rate corresponds to a contribution to the leakage current of the detector of $< 6.4 \times 10^{-19}$ A.

The present DM constraints extend to much smaller masses than searches based on noble gas detectors [9,33] and are competitive with those obtained with Si-based detectors [10–12]. In particular, the present limits are the most stringent ones on the kinetic mixing parameter $\kappa$ for dark photon masses between 6 and 9 eV/c$^2$. The better sensitivity of Ge compared to Si for $m_{\gamma} = 1$ eV/c$^2$ is due to the difference in gap energies. In this respect, Ge is a more favorable target for low-mass dark photon searches. For DM-electron scattering above 1 MeV/c$^2$, Si benefits from more favorable values of $f_c$.

The improvement by an order of magnitude of the detection threshold for electron recoils compared to [18] provides important constraints to understand the origin of the background limiting low-mass DM searches. Further progress in resolving the contributions of heat-only and single-pair events should come from an improvement of the energy resolution.
In the context of the EDELWEISS-SubGeV program, this will be achieved by upgrading the front-end electronics [36] and by operating the NTD sensor at lower temperature to improve its sensitivity. To improve the resolution after NTL amplification, the collaboration studies methods to better control the noise induced at large biases and develops detectors with alternative electrode schemes, such as double-sided vacuum electrodes. The collaboration also investigates possible techniques to tag single-charge events in order to reject the heat-only background.

In conclusion, the results obtained demonstrate for the first time the high relevance of cryogenic Ge detectors for the search of DM interactions producing eV-scale electron signals and represent an important milestone of the EDELWEISS-SubGeV program which aims at further probing a variety of DM models in the eV/c² to GeV/c² mass range.

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[25] This is larger than the 19% tail fraction from Fig. 1 due to the reduced K-line event rate (3 vs 15 mHz) in the postsearch activation sample compared to a constant Compton background.
[26] Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevLett.125.141301 for more detailed information about the detection efficiency and energy reconstruction of simulated signals.
[27] The rate observed at 25 eV ee would correspond to a background of $6 \times 10^3$ events/kg/day/keV at 0.68 keV if there is no contribution to the phonon signal from NTL amplification. This is a factor 3 below the background observed above ground at this energy in [18].
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