The purpose of the work is to develop an analytical method for calculating the effective ranges of structural parameters of the throttle part of the axial valve with the external location of the locking shell based on the proposed stochastic models of bubble formation at the initial stage of hydrodynamic cavitation. In contrast to the well-known engineering methods for choosing the conditional bore diameter for the designed control device constructed using the Pi-Buckingham theorem, this calculation method relies not only on gyrodynamic similarity criteria, but also on functional dependences for the laws of distribution of cavitation bubbles according to various characteristics (specific size bubbles, the degree of opening of the node “separator-external locking shell”). This takes into account a wide range of design and operating parameters, including the required valve capacity, as well as the physical and mechanical characteristics of the working medium. A block diagram of the calculation of the node “separator-external locking shell” for the specified axial valve is proposed. The influence of a set of design parameters for the “separator-external locking shell” assembly from the rational ranges of their variation obtained using the proposed analytical calculation algorithm on the size of cavitation bubbles is investigated. It has been established that when using the latest results in comparison with the values of parameters from irrational ranges of change, there is a tendency to reduce the ensemble average value of the diameter of the cavitation bubble by 1.95 times, when switching to a mode from 20% of the degree of separation of the separator to 80% of the opening of the throttle holes, the nominal valve capacity increases by 10.7 times. The results obtained illustrate the possibility of preventing an increase in the intensity of formation of cavities in the flow part of the control device already at the initial stage of the occurrence of cavitation.

Keywords: valve, separator, hydrodynamic cavitation, engineering method, parameter, stochastic model

INTRODUCTION

Improving engineering methods for calculating valves is a pressing issue in the field of pipeline fittings design. The use of valves (Emerson, 2020; Flowserve, 2020; Mokveld, 2020; Rust, 2020; Talis, 2020) in various branches of the chemical and oil and gas industry continues to expand. At the same time, the requirements for the main indicators of fluid transportation, such as throughput and expenditure characteristic of the valve, are constantly becoming tougher. The task of reducing the intensity of cavitation effects (Knapp et al., 1970; Franc and Michel, 2005; Xu et al., 2015) in the
flow part of the valve can be successfully solved by throttling fluid flows in designs (Emerson, 2020; Flowserve, 2020; Mokveld, 2020; Rust, 2020; Talis, 2020), which differ, for example, according to a number of characteristics: the shape of the throttle body, the number of throttle stages, the shape of throttle openings, the type of throttle channels, etc. Axial valves (Weevers, 1982; Peterman and Keithahn, 1987; Esveldt, 2012; Preston, 2018; Canjuga, 2019; Ziegler, 2019) provide a straight-line flow of fluid with minimal resistance when opened. Note that this type of valve is actively used in controlling flows, both liquid (Weevers, 1982; Peterman and Keithahn, 1987; Esveldt, 2012; Preston, 2018; Canjuga, 2019; Ziegler, 2019; Emerson, 2020; Flowserve, 2020; Mokveld, 2020; Rust, 2020; Talis, 2020) and gaseous media (Bian et al., 2019a,b; Cao and Bian, 2019; Emerson, 2020; Flowserve, 2020; Mokveld, 2020; Rust, 2020; Talis, 2020). Moreover, the system “perforated separator—internal piston” (Weevers, 1982; Peterman and Keithahn, 1987; Esveldt, 2012; Preston, 2018; Canjuga, 2019), in particular, with one (Peterman and Keithahn, 1987; Esveldt, 2012; Preston, 2018; Canjuga, 2019) or several throttle stages (Weevers, 1982) of throttling, when the internal piston, as a rule, is most widely used as a locking and regulating element. driven by rack and pinion (Preston, 2018; Canjuga, 2019) or crank mechanism. On the one hand, the shut-off and control system in the indicated design (Weevers, 1982; Peterman and Keithahn, 1987; Esveldt, 2012; Preston, 2018; Canjuga, 2019) allows separation of the fluid flows due to the formation of radial jets in the direction of the central axis of the valve, which contributes to the radial displacement of the cavitation bubbles formed in the central part of the separator and their accelerated removal from him. Thus, in the central part of the separator with one (Peterman and Keithahn, 1987; Esveldt, 2012; Preston, 2018; Canjuga, 2019) or several stages (Weevers, 1982) of throttling, the region of the working medium is displaced, which is subsequently subjected to the developed stage of cavitation, which prevents the collapse of bubbles near the inner surface of the cylindrical separator, and, consequently, its erosion. However, on the other hand, the internal arrangement of the locking element, in particular in the form of a piston (Weevers, 1982; Peterman and Keithahn, 1987; Esveldt, 2012; Preston, 2018; Canjuga, 2019), complicates the design of the sealing assembly, increases the energy costs of the drive and contributes to additional turbulization of the medium flow due to the location of the piston rod and spacers in the cavitation area. In Weevers (1982), another design version of the locking and regulating system in the form of a hollow cylindrical sleeve covering the separator was used. However, this design (Weevers, 1982) turned out to be quite complex and did not solve the problem of cavitation at small stages of valve opening. Note that the active use of various nozzle designs and the principle of swirling the working fluid flow are observed in Mokveld products (Mokveld, 2020), and similar technical solutions are used for gas liquefaction (Bian et al., 2019a,b; Cao and Bian, 2019). In particular, the analysis of design features of axial valves was performed in Lebedev et al. (2016, 2017a).

Regarding the methods for calculating the effective ranges of the design parameters of control valves, two approaches are most widespread: analytical estimation (Arzumanov, 1971, 1985; Blagov, 1990) using the Pi-Buckingham theorem (Buckingham, 1915; Misch et al., 2010) or numerical modeling for gaseous (Bian et al., 2019a,b; Cao and Bian, 2019) and liquid (Qu et al., 2015; Hou et al., 2017; Rudolf et al., 2017; Qiu et al., 2019; Tang et al., 2019) environments using ready-made software products (Ansys Inc, 2013, 2017). Moreover, the first approach requires a wide experimental base, and the second requires a long adaptation of the software product to the main factors influencing the course of the studied processes, including cavitation (Knapp et al., 1970; Franc and Michel, 2005; Xu et al., 2015), in a specific design. The formation of the theoretical base for the development of an engineering methodology for the analytical calculation of the desired parameters of control valves in this work is carried out on the basis of the stochastic approach by the energy method (Klimontovich, 2014). This choice (Kapranova et al., 2016c) from a variety of methods for describing the cavitation phenomenon, which include deterministic (Besant, 1859; Baron Rayleigh, 1911–1919; Plesset and Chapman, 1971; Chahine, 1994), stochastic (Volmer and Weber, 1926; Frenkel, 1946; Hsu, 1962; Lienhard and Karimi, 1981; Shin and Jones, 1993; Kwak and Kim, 1998; Ellas and Chambre, 2000) and combined Sokolichin et al., 1997; Koch et al., 2012; Seung and Kwak, 2017 approaches, is explained by the possibility of modeling differential functions of the distribution of the number of cavitation bubbles according to the characteristic features of the studied process (specific size of the bubbles, the degree of the medium flow of the valve) depending on the structural, operational parameters of the regulating device and the physico-mechanical properties of the working medium (Weevers, 1982).

Usually the stochastic approach (Volmer and Weber, 1926; Frenkel, 1946; Hsu, 1962; Lienhard and Karimi, 1981; Shin and Jones, 1993; Kwak and Kim, 1998; Ellas and Chambre, 2000) as models of homogeneous nucleation (Volmer and Weber, 1926; Frenkel, 1946; Lienhard and Karimi, 1981), their modifications with the introduction of the heterogeneity factor (Kwak and Kim, 1998; Ellas and Chambre, 2000), or heterogeneous nucleation (Hsu, 1962; Shin and Jones, 1993)] and combined one (Sokolichin et al., 1997; Koch et al., 2012; Seung and Kwak, 2017) suggest the use of the postulation of the differential distribution functions of cavitation nuclei by their size based on experimental dependences. Note that the deterministic approach (Besant, 1859; Baron Rayleigh, 1911–1919; Plesset and Chapman, 1971; Chahine, 1994) is usually implemented either when describing the behavior of a single bubble of variable radius, or in modified models taking into account additional factors of inertial, thermal, and diffusion nature. However, the latter approach is most relevant when applied to the estimation of the velocity regimes of growth of cavitation bubbles near the wall, including during numerical simulation (Qian et al., 2016).

The team of authors analyzed the design features of direct-flow type control valves (Lebedev et al., 2016, 2017a,b), methods for modeling the cavitation phenomenon (Kapranova et al., 2016c) and calculation of the main indicators of this process (Kapranova et al., 2016d,e), and also performed theoretical (Kapranova et al., 2016a,b, 2017, 2018a,b; Kapranova, 2018; Kapranova and Miadonye, 2019) and experimental (Esveldt, 2012; Lebedev et al., 2017a,b; Preston, 2018) studies of the initial...
stage of hydrodynamic cavitation with axisymmetric throttling of fluid flows, which made it possible to obtain a theoretical justification and experimental confirmation (Kapranova and Miadonye, 2019) of the possibility of reducing the intensity of formation of cavitation bubbles and the use of external locking shell. As a result of these studies, the authors proposed the design of an axial valve (Arzumanov, 1985; Lebedev et al., 2018) with a locking and regulating system “perforated separator—external locking cylinder-conical shell.” The specified design (Arzumanov, 1985; Lebedev et al., 2018) involves a coaxial arrangement of the separator and the movable external locking member, which has the form of hollow cylindrical shell (Figure 1). Thus, the throttle round holes of the fixed separator overlap when the cylindrical shell obeys along its outer cylinder-conical surface. This shell can be set in motion as a rack and a crank mechanism.

Thus, after solving a number of problems in developing stochastic models for the formation of cavitation bubbles in an axial valve separator by their size (Kapranova et al., 2016a, 2017, 2018a) and the degree of its opening (Kapranova, 2018; Kapranova et al., 2018b; Kapranova and Miadonye, 2019), after performing a series of comparative analysis (Kapranova and Miadonye, 2019) of the theoretical (Kapranova et al., 2016a, 2017, 2018a,b; Kapranova and Miadonye, 2019) and experimental results (Lebedev et al., 2017a,b) the next goal of studies of axisymmetric throttling of fluid flows is the development of engineering methods for calculating operational and design parameters of the separator-locking shell assembly.

METHODS

To ensure the effective operation of an axial valve with an external position of the locking member, an engineering procedure has been proposed for calculating a separator with round throttle holes. The purpose of the work is to develop a scientifically based method for calculating the effective ranges of the design parameters of the throttle part of the axial valve. Currently, the design of equipment (Hou et al., 2017; Qiu et al., 2019) subject to the effect of cavitation, as a rule, is based on the active use of ready-made software products (Tang et al., 2019), and as a result, has a numerical representation of the results (Rudolf et al., 2017) of their application in graphical or tabular form. Visualization of the studied process (Qu et al., 2013), performed by this method, has a high degree of visibility for a particular device, however, this requires the preliminary implementation of labor-intensive experimental validation (Qu et al., 2015). Such an approach often puts the designer in a dependent position on the level of development of numerical methods, on the completeness of taking into account in the finished software package the main factors of influence on the studied physical phenomena, requires a long adaptation of this software package to the specific regulatory requirements of the customer of control valves. In this presentation, preference is given to constructing an engineering methodology for calculating the main assembly of the valve using estimated analytical dependencies that allow us to analyze the mechanics of the behavior of the system of forming bubbles in the process of throttling the fluid flow. The theoretical basis for this calculation is stochastic modeling of the bubble formation process in the separator at the initial stage of hydrodynamic cavitation (Klimontovich, 2014; Kapranova et al., 2016a,b). Earlier, the authors used the stochastic approach with the equilibrium representation of the states of the energetically closed macrosystem (Klimontovich, 2014; Tang et al., 2019) within the framework of the Ornstein-Uhlenbeck random process (Kapranova et al., 2016b) to form the model of this process the bubble formation process in the separator at the initial stage of hydrodynamic cavitation. The proposed stochastic models (Kapranova et al., 2016a, 2017, 2018a,b; Kapranova, 2018; Kapranova and Miadonye, 2019) allowed us to obtain differential distribution functions of the number of cavitation bubbles formed during the initial stage of the evolution of hydrodynamic cavitation, according to their size (Kapranova et al., 2016a, 2017, 2018a) and the degree of opening of the axial valve (Arzumanov, 1971; Lebedev et al., 2017a,b). The performed experimental studies (Lebedev et al., 2017a,b) confirmed the possibility of reducing the intensity of hydrodynamic cavitation at its initial stage when using the modernized part of “separator-locking shell” of axial valve. In this case, a comparative analysis (Kapranova and Miadonye, 2019) of the obtained theoretical (Kapranova et al., 2016a, 2017, 2018a,b; Kapranova, 2018; Kapranova and Miadonye, 2019) and experimental (Lebedev et al., 2017a,b) results for the dependence of the differential distribution function of the number of bubbles $f_z(z)$ at the initial stage of hydrodynamic cavitation with a separator with round holes depending on the degree of their opening with using an external locking shell showed satisfactory convergence with a relative error not exceeding 13%. Note that the value of $z$ is determined by the ratio of the given position $z'$ for the movable shutter (external locking shell) along its axis to the conditional position $L$ corresponding to the length of the perforated part of the separator. The well-known classical method for calculating some rational parameters of a control valve (Arzumanov, 1971, 1985), which is actively used in various interpretations, including numerical ones, does not imply the use of functional dependencies for the laws of distribution of cavitation bubbles according to various characteristics, but it contains a reliable algorithm for the designer’s actions when choosing the type regulatory device, depending on the regulatory data of the customer. In this case, the basis of the calculation is a set of empirical dependences for the diameter of the nominal bore, the valve throughput on a number of operating parameters characterizing the movement of the fluid flow (maximum achievable fluid flow, pressure drop, etc.) and the main hydrodynamic similarity criterion (critical Reynolds number). An empirical analysis of the conditions for achieving a critical value of the cavitation coefficient as a doubled criterion of Euler similarity plays a decisive role in the choice of type of control device (Knapp et al., 1970; Franc and Michel, 2005; Xu et al., 2015; Kapranova et al., 2016e). The last operation is performed according to the critical value of the hydraulic resistance coefficient using graphical experimental material (Arzumanov, 1971, 1985; Blagov, 1990) at the stage of estimating the maximum value of the valve throughput in comparison.
with the routine. Thus, the application of the classical method for choosing the type of control device is associated with the application of the Pi-Buckingham theorem (Buckingham, 1915; Misic et al., 2010) in solving the scaling problem and reducing the number of constant parameters describing the process under study. As a result of the model (Kapranova et al., 2016a,b), the integral characteristics of the cavitation bubble were calculated. The expression obtained using model (Kapranova et al., 2016a) for calculating the average over the ensemble of the diameter \( D_{cb} \) for the macrosystem of cavitation bubbles (Kapranova et al., 2017; Kapranova, 2018) takes into account the physical and mechanical properties of the working medium, as well as the main design and operating parameters of the axial valve. In particular, the analysis of graphic material for the functional dependence of \( D_{cb} \) on the conditional diameter \( D_y \) and the corresponding throughput ability of the valve is presented in Kapranova A. B. et al. (2019). Another model (Kapranova, 2018; Kapranova et al., 2018b; Kapranova and Miadonye, 2019) made it possible to establish a connection between the critical value of the Reynolds number \( \text{Re}_{cr} \) in the case of a complete opening of the valve and its design parameters. So, these expressions for \( D_{cb} \) (Kapranova et al., 2017, 2018a) and \( \text{Re}_{cr} \) based on (Kapranova, 2018; Kapranova et al., 2018b; Kapranova and Miadonye, 2019), as well as the obtained expressions for the energy parameter of the stochastic model (Kapranova et al., 2018b) and the hydraulic resistance coefficient (Kapranova et al., 2018c) are used in the proposed engineering method for calculating the separator and constitute the main difference from the known approach (Arzumanov, 1971, 1985). Note that in practice, the identification of the cavitation region in the flow part of the control device is associated with the analysis of the dependence of the hydraulic resistance coefficient for the conditional flow area on the cavitation number \( k_C \), which is also reflected in this work.

RESULTS AND DISCUSSION

Selection of the Main Parameters of the Liquid Throttling Process in an Axial Valve With an External Locking Shell

We divide the whole set of parameters of the studied process of throbbing the fluid flow into several sets: for design parameters \( q \), for mode parameters \( \tau \), for additional \( \varphi \). In particular, the main structural parameters of the axial valve with the design of an external movable locking device (Lebedev et al., 2018) (Figure 1) include: \( q = \{ q_{k_1} = \text{const} \} \), \( k_1 = T, \rho_1 \) for the separator, external shells and corresponding parts of the housing: the diameter of the round throttle holes \( d_0 \), the arc distance between the holes in the same row \( S_{\varphi_1} \), the distance between the rows of these holes \( l_0 \), the thickness of the separator \( h \), the number of holes for one row \( u \), the number of these rows \( \varphi_2 \), respectively, the inner and outer diameters separator \( D_{out} \) and \( D_c \), the length of

![Figure 1](image-url)
its perforator of the left part $L$, the bevel angle for the cylindrical part of the shell $\alpha$, the inner diameter for the cylindrical part of the outer casing $D_{\text{out}}$, the outer diameter of the inner valve body $D_{\text{ch2}}$, the wall thickness of the inner and outer casing $\delta_1$ and $\delta_2$. Thus, the explicit representation of the set $\{q_k = \text{const}\}$ has the form

$$q = \{d_0, S_q, l_0, h, u_1, u_2, D_{\text{out}}, D_c, L, \alpha, D_{\text{cas}}, D_{\text{ch2}}, \delta_2\}, \quad k_1 = 13. \quad (1)$$

Set (1) is conveniently divided into three subsets for the main parameters of the separator $q_{11} = \{q_{k1} = \text{const}\}, k_1 = 1, \rho_1$, for the outer locking shell $q_{12} = \{q_{k2} = \text{const}\}, k_1 = 1, \rho_2$, and for the body $q_{13} = \{q_{k3} = \text{const}\}, k_3 = 1, \rho_3$ are the maximum attainable expenditure $Q_{1\max} ($m$^3$/h) of the liquid through the regulating device at a given value of the medium temperature $t_1$ (°C), the minimum pressure drop $\Delta P_{\min}$, the maximum pressure in the center of the bubble $P_{\max}$, which corresponds to the minimum value of its radius $r_{min}$ the saturated vapor pressure of the medium $p_s$, the velocity of the fluid in the pipeline $w$ then for $\{\tau_k = \text{const}\}$ we have

$$\tau = \{Q_{1\max}, t_1, \Delta P_{\min}, P_{\max}, r_{min}, p_s, w\}, \quad k_2 = 7. \quad (5)$$

The following additional parameters are taken into account:

$$\varphi = \{q_{k_0} = \text{const}\}, \quad k_3 = 1, \rho_3$$

$$\varphi = \{pl, p_g, p_s, v_1, \sigma, \gamma, k\}, \quad k_3 = 7. \quad (6)$$

describing the physical and mechanical properties of the medium: respectively, the density of the liquid $p_l$, gas $p_g$ and vapor $p_s$; kinematic viscosity of the liquid $v_1$ at a given value of its temperature $t_1$ (°C), surface tension coefficient $\sigma$, volumetric weight of the medium $\gamma$, adiabatic exponent $k$.

We make a selection of input $x_1 = \{x_1, k_1\}, \quad k_1 = 1, \rho_4$ and output $x_2 = \{x_2, k_2\}, \quad k_2 = 1, \rho_5$ parameters for the process of regulating fluid flows in the flow part of the axial valve

$$x_1 = \{Q_{1\max}, \delta_{\min}^{\Delta P_{\min}}, \delta_{\max}^{\Delta P_{\min}}, t_1, w\}, \quad k_4 = 5, \quad (7)$$

$$x_2 = \{\kappa_{\gamma y}\}, \quad k_5 = 1. \quad (8)$$

where the set $x_1$ is a subset of the operational parameters $\tau$ from (2); $\delta_{\min}^{\Delta P_{\min}}$ and $\delta_{\max}^{\Delta P_{\min}}$ are limits for $\Delta P_{\min}$; $\kappa_{\gamma y}$ is a required valve throughput.

When describing the block diagram (Figures 2, 3) for calculating the design parameters of the “separator-external locking shell” assembly of the axial valve, from the listed sets (2)–(8), it is necessary to select the following parameters:

- for input data input: sets $\varphi, x_1, x_2$, respectively, from (6) to (8); the set of initial values of a number of parameters from the subset $q_0 = \{q_{k_0} = \text{const}\}, \quad k_0 = 1, \rho_0$ for the set $q_0 = \{q_{k_0} = \text{const}\}, \quad k_0 = 1, \rho_0$ from (1)

$$q_0 = \{h^{(0)}, D_{\text{out}}^{(0)}, D_c^{(0)}, L^{(0)}, \alpha^{(0)}, D_{\text{cas}}^{(0)}, D_{\text{ch2}}^{(0)}\}, \quad k_0 = 7, \quad (9)$$

as well as the subset $\tau_1 = \{q_{k_21} = \text{const}\}, \quad k_21 = 1, \rho_{21}$ for the set of regime parameters $\tau$ from (5)

$$\tau_1 = \{r_{min}, p_s, w\}, \quad k_2 = 3. \quad (10)$$

- to search for the limits of change of parameters from $q$-set (1) in the form of the set of desired design parameters $q^* = \{q_{k_3} = \text{const}\}, \quad k_1 = 1, \rho_1$ for the designed axial valve elements (Figure 1) according to sets (2)–(4): for the separator $q_{11}^* = \{q_{k_11}^* = \text{const}\}, \quad k_11 = 1, \rho_{11}$, for the external locking shell $q_{12}^* = \{q_{k_12}^* = \text{const}\}, \quad k_12 = 1, \rho_{12}$ and for the body $q_{13}^* = \{q_{k_13}^* = \text{const}\}, \quad k_13 = 1, \rho_{13}$.

The proposed block diagram (Kapranova et al., 2019b) (Figures 2, 3) consists of 25 main blocks for calculating 13 effective values of the design parameters of the axial valve separator testing in calculating the example in Kapranova et al. (2020).

**Description of the Work Flowchart of the Engineering Methodology for Calculating the Parameters of These System of the Separator-External Locking Shell**

**Block 1** (Figure 2) includes the introduction of the parameters listed above: regime $\tau = \{\tau_k = \text{const}\}, \quad k_2 = 1, \rho_{23}$ from (5), including the input set $x_1$-set from (7); additional characteristics reflecting the physicom technological properties of the working medium and the gas-vapor system inside the bubble $\varphi = \{q_{k_0} = \text{const}\}, \quad k_3 = 1, \rho_{3}$ from (6); weekend $x_2$ from (8). In particular, according to the $x_1$-set from (7), the variation limits $\delta_{\min}^{\Delta P_{\min}}$ and $\delta_{\max}^{\Delta P_{\min}}$ are set for the minimum pressure drop $\Delta P_{\min}$ from (7) for a fixed value of the medium temperature $t_1$ (°C)

$$\delta_{\min}^{\Delta P_{\min}} \leq \Delta P_{\min} \leq \delta_{\max}^{\Delta P_{\min}} \quad (11)$$

**Block 2** (Figure 2) calculates the interval of variation in the maximum flow capacity of the valve $K_{x_1y_1}^{(1)} = [\delta_{\min}^{\Delta P_{\min}}, \delta_{\max}^{\Delta P_{\min}}]$ for given values of $\delta_{\min}^{\Delta P_{\min}}$ and $\delta_{\max}^{\Delta P_{\min}}$ from (11) taking into account the dependence $K_{x_1y_1} = \Delta P_{\min}$ (Azumanov, 1971), also used in (Kapranova et al., 2020)

$$\delta_{\min}^{\Delta P_{\min}} = \eta_1 Q_{1\max} \left(\frac{\gamma}{1,02 \times 10^{-5} \delta_{\max}^{\Delta P_{\min}}}\right)^{1/2}, \quad \delta_{\max}^{\Delta P_{\min}} = \eta_2 Q_{1\max} \left(\frac{\gamma}{1,02 \times 10^{-5} \delta_{\min}^{\Delta P_{\min}}}\right)^{1/2}, \quad (12)$$

where $Q_{1\max} ($m$^3$/h) is the maximum attainable flow rate of the fluid through the valve; $\gamma$ (g×cm$^3$/s$^2$) is the bulk density of
the liquid; \( \eta_1 \) and \( \eta_2 \) are safety factors in the range of at least 10–20% of the calculated value for the maximum throughput \( K_{v_{\text{max}}} \) according to Arzumanov (1971), for example, \( \eta_1 = 1.1 \) and \( \eta_2 = 1.2 \) (Kapranova et al., 2020); dimension for \( \delta_{\alpha_{\text{min}}} \) and \( \delta_{\Delta p_{\text{min}}} \) is Pa.

Using conditional block 3 (Figure 2), the condition of belonging of the required value of throughput \( K_{vy} \) for the valve to the obtained range of values is checked

\[
\delta_{K_{vy1}} \leq K_{vy} \leq \delta_{K_{vy1}}.
\]  

If inequality (13) is satisfied, the transition to block 4 follows; otherwise, it returns to block 2 (Figure 2) with the change of the safety factors \( \eta_1 \) and \( \eta_2 \) by 10–20%, respectively.

In block 4 (Figure 2) initial values are set:

- diameter of conditional passage \( D_y^{(0)} \) (m), as the nearest integer to the larger side \( \lceil d \rceil \) (“ceiling” \( d \))

\[
D_y^{(0)} = \lceil d \rceil,
\]  

(14)

- for the diameter of the pipeline \( d \) (m) according to Bian et al. (2019a)
\[ d = 1.88 \times 10^{-2} (Q_{1\text{max}}/w)^{1/2}, \]  

(15)

where the fluid velocity \( w \), for example, is usually taken for a water supply system \( w = 1.0 \) m/s, when supplied to a centrifugal pump \( w = 2.0 \) m/s, during transportation \( w = 3.0 \) m/s;

- for the design parameters described in sets (1), (9)

\[
q_{01} = \left[ d_{0}^{(0)}, S_{\phi 1}^{(0)}, h_{0}^{(0)}, u_{1}^{(0)}, u_{2}^{(0)}, h_{1}, u_{1}^{*}, u_{2}^{*}, D_{\text{out}}^{0}, D_{c}^{0}, L^{0}, \alpha^{0}, D_{\text{cas}}^{0}, D_{\text{ch}}^{0} \right], \\
k_{01} = 12
\]

(16)

using the following expressions (Kapranova, 2018; Kapranova et al., 2020): \( \delta_{2}^{(0)} = 0.1D_{y}^{(0)} \); \( h_{0}^{(0)} = \delta_{2}^{(0)} / 2; D_{\text{out}}^{0} = 1.1D_{y}^{(0)}; L^{0} = 2.2D_{\text{out}}^{0}; d_{0}^{(0)} = 0.14D_{\text{out}}^{0}; S_{\phi 1}^{(0)} = d_{0}^{(0)}; \]

\[ t_{0}^{(0)} = \left[ 3(d_{0}^{(0)} + S_{\phi 1}^{(0)}) - d_{0}^{(0)} \right] / 3; \]

\[ u_{2}^{0} = \pi D_{\text{out}}^{0} / (2d_{0}^{0}); u_{1}^{0} = (L^{0} - t_{0}^{(0)}) / (t_{0}^{(0)} + d_{0}^{0}); \]

\[ D_{c}^{0} = D_{\text{out}}^{0} + h^{(0)}; D_{\text{ch}}^{0} = 3D_{\text{out}}^{0}/2; D_{\text{cas}}^{0} = 2D_{\text{out}}^{0}; \alpha^{0} = \pi / 4 \]

and the condition \( h = D_{c} - D_{\text{out}} \) with a checkerboard arrangement of the throttle holes of the cylindrical separator. Note that when determining the values \( u_{1}^{0}, u_{2}^{0} \), the right-hand sides of the corresponding
expressions contain the integer parts of the indicated relations of quantities.

In block 5 (Figure 2), the critical value of the Reynolds number $Re_{cr}$ is determined when, when the inequality

$$Re_y \leq Re_{cr}, \quad (17)$$

cavitation-free flow of liquid in the valve is observed at a conditional value of the Reynolds number $Re_y$. In this case, the extremum condition is used

$$\left(\frac{dE_0}{dz}\right)|_{z=1} = 0, \quad (18)$$

for the energy parameter $E_0(z)$ with the value of the phase variable $z(u_2) = 1$, i.e., with full valve opening for a stochastic model of bubble formation at an early stage of hydrodynamic cavitation (Kapranova et al., 2018; Kapranova et al., 2018b; Kapranova and Miadonye, 2019). Here $z$ is the phase variable corresponding to the number of the throttle bore of the separator $n_2 = \frac{0}{u_2}$. The parameter $E_0(z)$ is determined by the expression for the energy $E_0(\xi, \eta, z)$ of the cavitation bubble at the moment of its stochasticization (when the trajectories of the formed bubbles acquire a random character), where $\xi$ and $\eta$ are the conditional values of the diameter of the cavitation bubble and the velocity of its center of mass. Condition (18) implies the approximation

$$\left(r_{m/} / [\psi_{10}[u_2(z)]]\right)^{1/2} \left(\begin{array}{l} v_L \left(r_{m/} / [\psi_{10}[u_2(z)]]\right) \end{array}^{-1/2} = 0, \quad (19)$$

which can be used as an algebraic equation for the value $Re_{cr}$ from (Kapranova, 2018; Kapranova et al., 2020)

$$Re_{cr} = \frac{32\rho_L k_L \kappa_{12(0)} \left(B_1 + s_2(0) + 4a_1 r_{min} \right)}{\left[\frac{2(1 - l_0)}{(2 - l_0)} - s_0(0) - s_0(0)\right]^2}. \quad (20)$$

Condition (19) contains the error function erf(μ) with argument μ. In the expressions (19), (20) it is indicated: $r_{m/}, v_L$ are the characteristic values of the radius of the bubble and the velocity of the fluid, respectively; $\psi_{10}(z) = r_{m/}[\tau_{11}(1) + \tau_{12}(z)(\tau_{12}(z))]$ according to Kapranova and Miadonye (2019); $\tau_{12}(z)$ is the dependence of the hydraulic resistance coefficient on the phase variable $z$ for the transition region of the fluid flow ($10 < Re < 10^4$), obtained in (Kapranova et al., 2018c)

$$\tau_{12}(z) = \frac{L z}{z_0} - \frac{1}{2} + s_2 + s_4 \left[\frac{90 s_0 s_4 (s_0 + s_6 z)}{2(2L - l_0)\zeta(z)} - \frac{1}{2}\right], \quad (21)$$

In (21) it is indicated: $\zeta(z)$ is the modified compression ratio of the jet from Kapranova et al. (2016a) with parameters $U_0 = 0.57; U_1 = 0.043; U_0 = 1.1$ from Arzumanov (1971); the coefficients $\tau_{11}(1), \tau_{12}(1), s_0, s_3, s_5, s_7, s_8(0), B_1, B_1, a_1, a_1$ due to Kapranova et al. (2018c) depend on the design parameters of the valve and the characteristics of the liquid-gas-vapor system, in particular $a_1 = 2x(a_1 p + a_1 p)/3$ Using expressions (14), (21) and the values described in block 4 (Figure 2) for the initial approximations of the design parameters for the set $q_0$ from (19), the following expression of the relationship between the design parameters is accepted

$$s_0(0) = l_0(0) + d_0'(0), \quad (22)$$

$$s_1(0) = \frac{4D_{out}}{\pi u_1(0) d_0(0)}, \quad (23)$$

$$s_2(0) = 64u_1(0) k_1(0) D_y(0)^2, \quad (24)$$

$$s_3(0) = 2 \left[\frac{D_{out}^2 - 2s_0(0)}{D_{ch2}^2} - \frac{D_{ch2}^2}{(D_y)}\right]^2, \quad (25)$$

$$s_4(0) = \frac{4u_1(0) k_1(0) (D_{ch2}^2)^2}{\pi d_0(0)^3}, \quad (26)$$

The physical and mechanical characteristics of the working medium $\rho_1, \rho_2, \rho_3$ from (25) correspond to the set $\varphi = \{d_{0}, const\}, k_3 = 1, \rho_3$ from (6). Expression (27) corresponds to the initial approximation for the hydraulic resistance function $\tau_{12}(z)$ on the phase variable $z$ from (21) (Kapranova et al., 2018c), taking into account the dependence of the degree of valve opening $z(u_2)$ on parameter $u_2$ with the equality of argument $u_2 = u_2(0)$ according to the accepted value $u_2(0)$ in block 4.

Block 6 (Figure 2) sets the 1st approximation for the conditional diameter $D_y(1)$ (m) using the empirical formula from (Arzumanov, 1971)

$$D_y(1) = (3.53 Q_{1\text{max}})/(v_1Re_{cr}), \quad (28)$$

where the values of $Q_{1\text{max}}$ ($\text{m}^3/\text{h}$) and $v_1$ ($\text{cm}^2/\text{s}$) are determined by the set (5); $Re_{cr}$ is the critical value of the Reynolds number from (20). The limits of change for the value $\delta_{D_y}^\text{min, max}$ of $D_y(1)$ (m) from (28)

$$\delta_{D_y}^\text{min, max} \leq D_y(1) \leq \delta_{D_y}^\text{max}, \quad (29)$$
are established taking into account (12) for $\delta_{K_{y21}}^{\min}$, $\delta_{K_{y21}}^{\max}$, in the form

$$
\delta_{D_y}^{\min} = \left(\frac{4 \delta_{K_{y21}}^{\min} S_{12}^{(0)} [z(u_z^{(0)})]}{10^4 \pi m_0}\right)^{1/2},
$$

$$
\delta_{D_y}^{\max} = \left(\frac{4 \delta_{K_{y21}}^{\max} S_{12}^{(0)} [z(u_z^{(0)})]}{10^4 \pi m_0}\right)^{1/2},
$$

(30)

where the value $S_{12}^{(0)} [z(u_z^{(0)})]$ is calculated using (27). The expressions in (30) were obtained using the well-known empirical relationship between the coefficients of the transmission capacity of the regulating device and hydraulic resistance (Arzumanov, 1985; Blagov, 1990) at the value of the coefficient $m_0 = 5.04$.

Service block 7 (Figure 2) compares the calculated critical value of the Reynolds number $Re_{cr}$ from (20) with the characteristic value of this criterion for liquid flow in cavitation-free mode according to the recommendations from Arzumanov (1971) (if which is not met, go to block 11, Figure 2) $Re_{cr} \leq 2 \times 10^5$. If this inequality is true, in block 8 (Figure 2), correction coefficients $\psi_1$, $\psi_2$ for the viscosity of the working medium are calculated similarly to the recommendations from Arzumanov (1971) for the limits of the valve throughput $K_{max}^{(2)} \in [\delta_{K_{y21}}^{\min}, \delta_{K_{y21}}^{\max}]$ taking into account (12), (28), (20) for the values $\delta_{K_{y21}}^{\min}, \delta_{K_{y21}}^{\max}$, $Re_{cr}$, as well as the values of initial approximations adopted in block 4 (Figure 2) for the design parameters $D_y^{(1)}, \delta_0^{(0)}, u_z^{(0)}$, in the form

$$
\psi_1 = 1.07 \times 10^{-2} \frac{\delta_{K_{y11}}^{\min}}{\omega_y [z(u_z^{(0)})]} \left[\frac{\pi \left(D_y^{(1)} + \delta_0^{(0)}\right)}{Re_{cr} D_y^{(1)}}\right]^{1/2},
$$

$$
\psi_2 = 1.07 \times 10^{-2} \frac{\delta_{K_{y11}}^{\max}}{\omega_y [z(u_z^{(0)})]} \left[\frac{\pi \left(D_y^{(1)} + \delta_0^{(0)}\right)}{Re_{cr} D_y^{(1)}}\right]^{1/2},
$$

(31)

The expressions in (31) contain the value of the conditional section area $\omega_y [z(u_z^{(0)})] = \pi u_1^{(0)} u_2^{(0)} (d_0^{(0)})^2 z(u_z^{(0)})/4$ (m$^2$) depending on the degree of valve opening $z$ according to the parameter values $d_0^{(0)}$, $u_1^{(0)}$, $u_2^{(0)}$ accepted in block 4 (Figure 2). Therefore, in block 9 (Figure 2), taking into account (12), (31), a new range of variation in the valve throughput can be determined $\delta_{K_{y21}}^{\min} = \psi_1^{\min} \delta_{K_{y11}}^{\min}, \delta_{K_{y21}}^{\max} = \psi_2^{\max} \delta_{K_{y11}}^{\max}$.

The conditional block 10 (Figure 2) checks the condition that the required valve throughput $K_{y2}$ belongs to a new range of values $\delta_{K_{y21}}^{\min}, \delta_{K_{y21}}^{\max}$ using the following inequality $\delta_{K_{y21}}^{\min} \leq K_{y2} \leq \delta_{K_{y21}}^{\max}$ similar to (13). If the last inequality is true, the transition to block 11 (Figure 2) is carried out, in case of its injustice—return to block 2 with a change in the values $n_1$ and $n_2$ of the safety factors and, accordingly, by 10–20%.

In block 11 (Figure 2), the values of the first approximations are estimated $d_0^{(1)}$, $u_2^{(1)}$, $L_j^{(1)}$, $\delta_0^{(1)}$, $j = 1, 2$ for the limits of variation of the following design parameters of the separator $d_0^{(1)}, u_2^{(1)}, L_j^{(1)}$ according to the inequalities:

$$
d_0^{(1)} \leq d_0^{(1)} \leq d_0^{(1)} \leq u_2^{(1)} \leq u_2^{(1)} \leq u_2^{(1)} \leq L_j^{(1)}, L_j^{(1)} \leq L_j^{(1)} \leq L_j^{(1)},
$$

using a system of equations including:

- the expression $\sigma_y z(u_2^{(1)})/\sigma_y z(u_2^{(1)}) = 1$, which reflects the condition for linear profiling of the dependence $\sigma(z)$ of the throughflow characteristic of the control device on the degree of its opening according to the definition of $\sigma(z) = K_{y2}[z(u_2^{(1)})/K_{y2}[z(u_2^{(1)})]]$, $n_2 = 0, u_2^{(1)}$;

- extremum condition for the hydraulic resistance coefficient $\sigma_2(z)$ from (21) with respect to the parameter $u_2^{(1)}$ when the valve is fully open when the condition $z(u_2^{(1)}) = 1$ is satisfied, in the form

$$
(d_\xi_{12} du_2^{(1)}) z(u_2^{(1)}) = 1,
$$

(32)

- two geometric relations between the sought parameters $d_0^{(1)}, u_1^{(1)}, u_2^{(1)}$, $L_j^{(1)}$ taking into account the checkerboard arrangement of the throttle holes on cylindrical surface of the separator

$$
L_j^{(1)} = u_2^{(1)} \left[\frac{l_0^{(1)} + d_0^{(1)}}{d_0^{(1)}} + d_0^{(1)} + l_0^{(1)} / 2,\right.
$$

(33)

The solution of system (32), (33) is accompanied by the expansion of the first two equations from those listed in the Maclaurin series with respect to unknowns corresponding to the parameter values $u_2^{(1)}$, $d_0^{(1)}$ to terms of order $O(u_2^{(1)}), O(d_0^{(1)})$, then the values $u_2^{(1)}$, $d_0^{(1)}$ take

$$
u^{(1)} = 2 \left(\frac{l_0^{(1)}}{d_0^{(1)}} + d_0^{(1)}\right)^2, j = 1, 2,
$$

(34)

$$
\delta_0^{(1)} \leq 2 \pi \left(\frac{2 r^{(1)} y_{(1)}}{2 r^{(1)} y_{(1)}}\right)^2, j = 1, 2,
$$

(35)

$$
l_0^{(1)} = \left[\frac{3}{2} \delta_0^{(1)} + \delta_0^{(1)} - d_0^{(1)} / 2, L_j^{(1)} = u_2^{(1)} \left(\frac{l_0^{(1)} + d_0^{(1)}}{d_0^{(1)}} + l_0^{(1)}\right), j = 1, 2,
$$

(36)

where $r^{(1)} y_{(1)}$ correspond to the formula (24); parameters $d_0^{(1)}, l_0^{(1)}, \delta_0^{(1)}, S_{y_{(1)}}^{(1)}$—to the expressions adopted in block 4 (Figure 2), taking into account $\delta_0^{(1)}$, $\delta_0^{(1)}$, $\delta_0^{(1)}$—the limits of change of the value $D_y^{(1)}$ (m) from (29). Note that the right-hand side of (34) contains an integer value from the corresponding relation.

In the next block 12 (Figure 2), the calculation $\pi_2^{(1)}, d_0^{(1)}, L_j^{(1)}, l_0^{(1)}$ is carried out of the required parameters.
Let $d_0, u_2, L, l_0$ as averaged values $d_0^{(1)}, u_2^{(1)}, L_0^{(1)}, l_0^{(1)}$ from the obtained boundary expressions (34)–(36):

$$
\bar{u}_2^{(1)} = \left[ \frac{u_2^{(1)} + u_2^{(2)}}{2} \right], d_0^{(1)} = \frac{d_0^{(1)} + d_0^{(2)}}{2},
L^{(1)} = \frac{L_1^{(0)} + L_2^{(0)}}{2},
$$

(37)

Note that in (37) for $d_0^{(1)}$ only the integer value of the obtained right-hand side is also taken.

**Block 13 (Figure 2)** is designed to estimate the value of the first approximation of the parameter $S^{(1)}_V$ using the formula

$$
S^{(1)}_V = \pi D^{(1)}_{out}/\pi^{(0)} - d_0^{(1)},
$$

where the inner diameter $D^{(1)}_{out}$ of the separator according to (35) and the accepted approximations in blocks 4, 6 (Figure 2) is determined by the limits of change $\delta^{min}_{D_y}, \delta^{max}_{D_y}$ for the value $D_s^{(1)}$, then $D^{(1)}_{out} = 1.1(\delta^{min}_{D_y} + \delta^{max}_{D_y})/2$.

**Block 14 (Figure 2)** includes the calculation of the second approximation for the inner diameter of the separator $D^{(2)}_y$ using the corollary from the extremum condition (18) for the energy parameter $E_{02}(z)$ from the stochastic model of bubble formation at an early stage of hydrodynamic cavitation (Kapranova et al., 2016b, 2018a) in the form

$$
\begin{align*}
&\left\{ \frac{d}{dz} \left[ \frac{v_L}{\pi L^{(1)}} \exp \left( -\frac{\psi_{10}(z)}{r_m} \right) - \frac{1}{2} \left( \frac{r_m}{\psi_{10}(z)} \right)^{1/2} \right] \right\}_{z=1} = 0, \\
&\text{erf} \left[ \frac{v_L}{\pi L^{(1)}} \left( \frac{\psi_{10}(z)}{r_m} \right)^{1/2} \right]_{z=1} = 0,
\end{align*}
$$

(38)

Given the form of the function $\psi_{10}(z)$ described in block 5 (Figure 2), for the desired parameter value, condition (38) yields the value of the desired structural parameter

$$
D^{(2)}_{out} = \frac{3}{4B_3 B_5 S^{(1)}_V} \left( L^{(1)} - l_0^{(2)} \right)
$$

(39)

where according to the expressions adopted in blocks 4, 5, 12 (Figure 2) for $D^{(0)}_0, D^{(0)}_{out}, \alpha^{(0)}_c, \beta^{(0)}_{12}, \alpha^{(0)}_h, l_0^{(1)}$, as well as the expressions (33), (36), (37) for $d_0^{(1)}, u_2^{(1)}, L^{(1)}, D^{(1)}_y, \bar{u}_2^{(1)}, S^{(1)}_V$ are indicated: $D^{(1)}_y = (\delta^{min}_{D_y} + \delta^{max}_{D_y})/2$, $B_3 \equiv \exp(v_L^{(1)} l_0^{(1)} a_1^{(1)}, B_4 \equiv s_2^{(1)} + s_1^{(0)} [L^{(1)} - l_0^{(1)} - 1/2], B_5 \equiv 2s_0^{(1)} [s_0^{(1)} + s_1^{(0)}]/\pi u_2^{(1)} d_0^{(2)}, B_6 \equiv N_0 - S_5^{(0)} [s_0^{(0)} + s_1^{(0)}]/4, B_7 \equiv 6s_0^{(1)} a_1^{(1)} [H_0^{(1)} d_0^{(1)}]/90s_0^{(1)} = \pi \left( \frac{1}{d_0^{(1)}} \right)^{1/2}, s_1^{(0)} = \frac{64 \pi^{(1)} H_0^{(1)} (D^{(1)}_y)^2}{Re_{Fr}},
$$

(40)

(41)

In block 15 (Figure 2), to determine the first approximation of the bevel angle for the cylindrical part of the shell $\alpha^{(1)}$, we also apply the corollary from the extremum condition (18) for $E_{02}(z)$ from the stochastic model of bubble formation at an early stage of hydrodynamic cavitation (Kapranova, 2018; Kapranova et al., 2018b; Kapranova and Miadonye, 2019) in form

$$
\begin{align*}
&\left[ \frac{v_L}{\pi L^{(1)}} \exp \left( -\frac{\psi_{10}(z)}{r_m} \right) - \frac{1}{2} \left( \frac{r_m}{\psi_{10}(z)} \right)^{1/2} \right]_{z=1} = 0,
&\text{erf} \left[ \frac{v_L}{\pi L^{(1)}} \left( \frac{\psi_{10}(z)}{r_m} \right)^{1/2} \right]_{z=1} = 0.
\end{align*}
$$

(42)

Therefore, according to (42), the value of the desired structural parameter is determined by the expression

$$
\alpha^{(1)} = \frac{s_0^{(1)} \left( s_0^{(1)} + s_0^{(2)} \right)}{20 \pi \pi_{V_1} (L^{(1)} - l_0^{(2)})},
$$

(43)

$$
\theta_1 = \frac{U_0}{U_1} \frac{1 - \frac{1}{2} \left( \frac{r_m}{\psi_{10}(z)} \right)^{1/2}}{1 - \frac{1}{2} \left( \frac{r_m}{\psi_{10}(z)} \right)^{1/2}}.
$$

(44)

$$
\theta_2 = \frac{\pi^{(1)}_{V_1}}{900 \pi^{(1)}_{V_2}} \left[ (D_{out}^{(0)} - 2 \pi^{(1)}_{V_2})^2 - (D_{out}^{(0)})^2 \right]^{1/2},
$$

(45)

To calculate the values $s_1^{(0)}, S_6^{(1)}, D_{out}^{(0)}, D_{out}^{(2)}, D_{out}^{(3)}, D_{out}^{(2)}, D_{out}^{(3)}, D_{out}^{(3)}$, in (43)–(45), the formulas are used, which are contained in blocks 4, 5 (Figure 2), as well as expressions (27), (40), (41). In conclusion, we determine the first approximation of the following parameters:

$$
\delta^{(2)}_2 = 0.1 D^{(2)}_y, h^{(1)} = \delta^{(1)}_2 / 2, D^{(2)}_c = h^{(1)} + D^{(2)}_c = 3 D^{(2)}_c / 2, D^{(2)}_{out} = 2 D^{(2)}_{out}.
$$
In block 16 (Figure 3), the value for the hydraulic resistance coefficient is calculated according to (21) and the formulas from (Kapranova et al., 2018c)

\[
\zeta_\gamma(z(\pi_2^{(1)})) = \left(1 - \frac{s_1^{(0)}}{2} \right) + s_1^{(1)} + \frac{1}{2} \left[ \pi_1^{(1)} \left( \frac{z(\pi_2^{(1)})}{\pi_0} - s_2^{(1)} \right) \right] ^2, \tag{46}
\]

where the compression ratio of the jet, in contrast to (26), is equal to

\[
e^2[z(\pi_2^{(1)})] = U_0 + U_1/(2 - f(\cdot)^{(1)} - s_2^{(1)})[\pi_0 + s_6^{(1)} z(\pi_2^{(1)})]/2, \tag{47}
\]

and the constants \(s_j^{(0)}, j = 1, 7 \) correspond to the expressions from block 14 (Figure 2).

In block 17 (Figure 3) calculates the critical value for the coefficient of hydraulic resistance \(\zeta_\gamma^*\) from the condition of achieving the minimum value for the ensemble average diameter of the cavitation bubble \(D_\delta\) according to Kapranova et al. (2017, 2018a,c), Kapranova A. B. et al. (2019), which corresponds to the following condition

\[
\frac{v_l}{\pi^{1/2}} \exp \left( - \frac{C_4^{1/2}}{E_{01} r_m} \right) - \frac{1}{2} \left[ \frac{E_{01}}{\pi_1^{(1)}} \right]^{1/2} \text{erf} \left( \frac{v_l}{\pi_1^{(1)}} \right)^{1/2} = 0. \tag{48}
\]

In condition (48), the coefficients \(E_{01}, C_4, 1\) (1) from the stochastic model (Kapranova et al., 2016a), which describes the process of formation of a bubble system at the initial stage of hydrodynamic cavitation in a control device, depend on the physical and mechanical properties of the working medium (including the density of the liquid, gas and vapor, and kinematic viscosity fluid) at a given value of its temperature, surface tension coefficient, volumetric weight of the medium, adiabatic index) and the desired value \(\zeta_\gamma^*\), then where indicated: \(\zeta_\gamma^* = 2\pi_0 r_m (\theta_2/2 + a_1 r_m \delta_2^{1/2}/k_1 - 4/3)/(3k_2^{1/2} l_2), \theta_2 = \theta_2 r_m + k_1\rho_2 r_m / (3k_2^{1/2} l_2), k_0 = 108\rho_2 r_m / k_1, \theta_2 = 12\sqrt{3}\pi_0 r_m (\theta_2 r_m / (27\rho_2 k_1) - 2\pi_1 r_m (\pi_0 r_m / E_01)^{1/2}, m_0 = 5.04, \pi_0 r_m / (27\rho_2 k_1 - 28\pi_1 r_m (\pi_0 r_m / E_01)^{1/2}, \theta_2 = \pi_0 r_m / (2(3k_2^{1/2} l_2) / (4\pi\exp(-1))/4\exp(-1)).

In conditional block 18 (Figure 3), a possible manifestation of a cavitation effect in the flow part of the valve is checked. Fulfillment of the following condition \(\zeta_\gamma^* \leq \zeta_\gamma\) leads to a graphical estimation of the cavitation coefficient \(k_c\) in block 19 (Figure 3) from empirical reference data (Arzumanov, 1971) for the critical value of the coefficient of hydraulic resistance \(\zeta_\gamma^*\) obtained in block 17 (Figure 3). Otherwise, when the inequality \(\zeta_\gamma^*>\zeta_\gamma\) holds, it returns to block 4 (Figure 2), associated with setting the critical value of the Reynolds number \(Re_c\) and changing the value of \(D_{\delta0}\) in (14).

In the next block 20 (Figure 3), the calculation is performed:

- critical (maximum permissible) pressure drop \(\Delta p_{\max}^* = k_{C_{\max}} (p_1 - p_{H1})\) during the regime of fluid movement with a critical value of \(k_{C_{\max}}\) for the cavitation coefficient \(k_c\), where \(p_1\) (kgf/cm²) is the absolute fluid pressure to the control valve at its maximum flow rate; \(p_{H1}\) (kgf/cm²) is absolute pressure of saturated steam at temperature \(t_1\) (°C);
- valve capacity in cavitation operation according to the well-known formula (Arzumanov, 1971, 1985)

\[K_{\text{max}} = \eta_{12} Q_{1\text{max}} (\gamma / \Delta p_{\max}^{1/2})\]

with a safety factor of \(\eta_{12}\).

Conditional block 21 (Figure 3) checks one of two inequalities:

- for differential pressure \(\Delta p_{\min} \geq \Delta p_{\min}\)
- for valve capacity \(K_{\text{max}} \) and the required value \(K_{\gamma}\) when \(K_{\text{max}} \leq K_{\gamma}\).

If these inequalities are true, the calculation can be completed with the transition to blocks 24 and 25 (Figure 3) to select and display the desired parameters of the separator. Otherwise, it is required to select a valve in the subsequent block 22 (Figure 3) in order to fulfill the condition for the conditional throughput from block 23 (Figure 3) according to the inequality

\[K_{\gamma} \geq K_{\text{max}}\]

where \(n_2\) is the safety factor within at least 10–20% of maximum value, i.e., in the range (1.1–1.2) units, and then return to block 2 (Figure 2).

Thus, in block 25 (Figure 3), the desired structural parameters of the designed axial valve separator are output in the form of the set \(\{q_1 = const\}, k_1 = 1, \delta_i\) according to the set

\[q = \{q_{k_{\gamma}} = const\}, k_1 = 1, \delta_i, \text{ from (1) when choosing the desired parameters, performed in block 24 (Figure 3)\}

\[q^* = \{d_0, S, r_0, l_0, h, u_1, u_2, D_{out}, D_{cas}, L, \alpha, D_{cas2}, D_{ch}, \delta_{ch}^2\}, \tag{49}\]

Moreover, in the set (49) the following approximations are used:

\[d_0 = d_0^{(1)}, S_{ch} = S_{ch}^{(1)}, l_0 = l_0^{(2)}, u_1 = u_1^{(1)}, u_2 = u_2^{(1)}, D_{out} = D_{out}^{(2)}, D_{cas} = D_{cas}^{(2)}, L = L^{(1)}, \alpha = \alpha^{(1)}, D_{cas2} = D_{cas2}^{(1)}, D_{ch} = D_{ch}^{(1)}, \delta_{ch}^2 = \delta_{ch}^{(2)}\]

For the diameter of the radial throttle holes; the diameter of the round throttle holes \(d_0\), the arc distance between the holes in the same row \(S_{ch}\), the distance between the rows of these holes \(l_0\), the thickness of the separator \(h\), the number of holes for one row \(m_1\), the number of these rows \(u_2\), respectively, the inner and outer diameters separator \(D_{out}\) and \(D_{ch}\), the length of its perforator of the left part \(L\), the bevel angle for the cylindrical part of the shell \(\alpha\), the inner diameter for the cylindrical part of the outer casing \(D_{cas2}\), the outer diameter of the inner valve body \(D_{ch}\), the wall thickness of the inner and outer casing \(\delta_{ch}^2\).

The Influence of a Set of Design Parameters From the Rational Ranges of Their Change for the Node “Separator-Locking Shell” on the Size of Cavitation Bubbles

From a practical point of view, of particular interest is the analysis of the influence of the desired set of design parameters from the rational ranges of their change for the node “Separator-Locking Shell” on the size of cavitation bubbles.
parameters from rational ranges of their change for the “separator-external locking shell” unit on the size of cavitation bubbles, as a reflection of the result of an engineering calculation on the nature of the course of the initial stage of hydrodynamic cavitation in the flow part of the designed control device.

The described engineering methodology from sections Selection of the Main Parameters of the Liquid Throttling Process in an Axial Valve With an External Locking Shell, Description of the Work Flowchart of the Engineering Methodology for Calculating the Parameters of These System of the Separator-External Locking Shell was tested in Kapranova et al. (2020) using the example of the calculation of the “separator-external locking shell” assembly of an axial valve with a regulated value of the valve throughput $K_{vy}$ was $6 \text{ m}^3/\text{h}$ when choosing water as the working medium and the following parameters of the throttling process: $Q_{max} = 0.5 \text{ m}^3/\text{h}$; $\Delta P_{min} = 0.90 \text{ kPa}$; $\rho_l = 10^3 \text{ kg/m}^3$; $t_1 = 30^\circ \text{C}$; $v_1 = 0.81 \times 10^{-2} \text{ cm}^2/\text{s}$; $\sigma = 7.28 \times 10^{-4} \text{ H/m}$; $w = 0.43 \text{ m/s}$; $r_{min} = 10^{-3} \text{ m}$; $\rho_{max} = 1.3 \times 10^5 \text{ kg/m}^3$; $\rho_1 = 10^{-3} \text{ Pa}$; $\rho_g = 1.205 \text{ kg/m}^3$; $\rho_s = 1.44 \times 10^{-2} \text{ kg/m}^3$ and adiabatic index $k = 1.3$. According to the calculation example performed in Kapranova et al. (2020) based on the engineering method (Kapranova et al., 2019b) described in this paper, with $K_{vy} = 6 \text{ m}^3/\text{h}$; $Re_p = 5209.58$; $\zeta_v = 0.119$ obtained rational ranges of changes of the desired parameters, in particular, the average value of $d_0$ from the specified range is $d_0^{(1)} = 5.05 \times 10^{-3} \text{ m}$ with a separator outlet diameter of $D_{out}^{(2)} = 4.19 \times 10^{-2} \text{ m}$ and the length of its perforated part $L^{(1)} = 8.21 \times 10^{-2} \text{ m}$ with the number of rows of throttle holes $n_2^{(1)} = 7$ for $n_1^{(0)} = 12$ pieces in each and the distance between these rows $l_0^{(1)} = 5.84 \times 10^{-3} \text{ m}$. Moreover, additional design parameters of the separator-external locking shell assembly correspond to the following effective values: separator thickness $h^{(1)} = 2.11 \times 10^{-3} \text{ m}$; its outer diameter $D^{(1)} = 4.55 \times 10^{-2} \text{ m}$; inner diameter for the cylindrical part of the outer casing $D_{end1} = 8.69 \times 10^{-2} \text{ m}$; the outer diameter of the inner valve body $D_{int} = 6.25 \times 10^{-2} \text{ m}$; wall thickness of the inner and outer shell $\delta_2 = 4.22 \times 10^{-3} \text{ m}$; bevel angle for the cylindrical part of the shell $a^{(1)} = 44.8^\circ$. The indicated values for the set of sought-for structural parameters $q_1^* = \{q_1^* = \text{const}\}$, $k = 1, \delta_1$ from expressions (49) and (50) allow, by analogy with the approach from Kapranova A. B. et al. (2019), based on (Kapranova et al., 2017, 2018a) to analyze the dependence $D_{db}(D_n, K_{vy})$ between the ensemble average value of the diameter $D_{db}$ for the macro-system of cavitation bubbles, the conditional diameter $D_n$ and the corresponding throughput of the $K_{vy}$ valve for its opening degree $2$ (Figures 4A,B).

The values of $D_{dbj}$, $j = 1, 4$ for the ensemble-average diameter of cavitation bubbles for various indicators of the degree of opening of the separator $z = \{0.2, 0.5, 0.8, 1.0\}$ are determined by the position of the end points of the lines for graphs 1–4 according to Figure 4A. Additionally, as a more comprehensive three-dimensional illustration, the dependence $D_{db}(D_n, K_{vy})$ in Figure 4B is presented. An analysis of the results showed that the transition from mode 1 of the separator with a degree of opening of 20% to mode 3 with 80% opening of the throttle openings is accompanied by an increase in the conditional throughput of the valve $K_{vy}$ by 10.7 times (as the ratio $K_{vy3}/K_{vy1}$), and in the case of the transition from mode 3 to full opening (mode 4), the ratio $K_{vy4}/K_{vy3} = 1, 4$. For comparison, we note that the case considered in Kapranova A. B. et al. (2019) for other values of the design parameters of the separator-external locking shell assembly that are not related to the rational ranges of their changes leads to the following relations $K_{vy3}/K_{vy1} = 2.1$ and $K_{vy4}/K_{vy3} = 1.4$. In addition, according to Figure 4A, a decrease in the size of the resulting bubbles is noted in $D_{db1}/D_{db4} = 1.35$ times from the range of the ensemble average diameter of the cavitation bubble $D_{db} = (0.74 - 1.0) \times 10^{-3} \text{ m}$ against the case from Kapranova A. B. et al. (2019), when $D_{db1}/D_{db4} = 1.12$ from the range $D_{db} = (1.6 - 1.8) \times 10^{-3} \text{ m}$. Moreover, a comparison of the results presented in Figure 4A and in Kapranova A. B. et al. (2019) showed that there is a tendency to decrease the $D_{db}$ value by 1.95 times when taking into account the rational ranges of changes in the desired design parameters $q_1^* = \{q_1^* = \text{const}\}$, $k = 1, \delta_1$ obtained in this article.

**KEY FINDINGS AND RESULTS**

The proposed block diagram consists of 25 main blocks for calculating 13 effective values of the design parameters of an axial valve separator. For example, the required parameters include: diameter of round throttle holes $d_0$, arc distance between the holes in one row, distance between rows of these holes, separator thickness, number of holes for one row, number of these rows, diameter of the outlet of the separator, its perforated part length, bevel angle for the cylindrical part of the shell, etc. Specified operating parameters are the maximum attainable fluid flow through the regulating device at a given value of the medium temperature, the minimum pressure drop, the maximum pressure in the center of the bubble, which corresponds to the minimum value of its radius, the saturated vapor pressure of the medium, the velocity of the fluid in the pipeline. The input parameters for the calculation are the maximum attainable flow rate of the medium, the temperature of the medium, the limits of variation of the minimum pressure drop and the velocity of the fluid in the pipeline. The output parameter is the required valve capacity $K_{vy}$. The block diagram (Figures 2, 3) proposes a phased calculation of various approximations of the desired design parameters depending on the selected intervals for changing the maximum value of the valve capacity. The indicated intervals are refined three times when taking into account the required value of $K_{vy}$ throughput with the choice of safety factors. The first time this is done at specified intervals for changing the minimum pressure drop, the second after calculating $Re_p$ based on (Kapranova, 2018; Kapranova et al., 2018b; Kapranova and Miadonye, 2019) to determine the correction factors for the viscosity of the medium, the third after evaluating the hydraulic resistance coefficient $\zeta_v^*$ (Kapranova et al., 2018c) from the minimum condition values of $D_{db}$ (Kapranova et al., 2017, 2018a, 2019a). Note that the
calculation of the conditional flow area for the control valve separator depends on the configuration of the throttle holes, which significantly affects the application of the expressions proposed in the method according to the models (Kapranova et al., 2018a,b,c; Kapranova and Miadonye, 2019). For example, this is reflected when using expressions (20)–(28) in blocks 5, 6 (Figure 2) for the critical value of the Reynolds number $\text{Re}_{cr}$, when choosing the first approximation for the conditional diameter $D_y^{(1)}$, and therefore, when calculating the value of the hydraulic resistance coefficient, including the critical $\zeta^*$ (blocks 17 and 18, Figure 3), etc. An analysis of the obtained critical value of the Reynolds number in comparison with the characteristic value from Kapranova et al. (2020) allows us to assess the need for additional consideration of the viscosity of the working medium using correction factors and to clarify the limits of change of the device throughput coefficient when setting the next approximation of the valve design parameters to ensure its effective operation according to the regulatory value $K_{vy}^\prime$. The work of the proposed engineering calculation method (sections Selection of the Main Parameters of the Liquid Throttling Process in an Axial Valve With an External Locking Shell, Description of the Work Flowchart of the Engineering
Methodology for Calculating the Parameters of These System of the Separator-External Locking Shell is illustrated by the example of comparative analysis (section The Influence of a Set of Design Parameters From the Rational Ranges of Their Change for the Node "Separator-Locking Shell" on the Size of Cavitation Bubbles) for the ensemble average diameter of the cavitation bubbles formed in the "separator-external locking shell" assembly with the external arrangement of the latter in the design of the control valve, depending on taking into account the values of design parameters from rational and irrational ranges of their change.

Thus, summarizing the results of this study leads to the following main conclusions and results:

- In the presented engineering method for calculating the main structural parameters (sections Selection of the Main Parameters of the Liquid Throttling Process in an Axial Valve With an External Locking Shell, Description of the Work Flowchart of the Engineering Methodology for Calculating the Parameters of These System of the Separator-External Locking Shell) for the direct-flow type apparatus (Lebedev et al., 2018), the following facts received their practical application:
  
  1. Design analysis of the design features of direct-flow type control valves (Lebedev et al., 2016, 2017a,b), methods for modeling the cavitation phenomenon (Kapranova et al., 2016c) and calculation of the main indicators of this process (Kapranova et al., 2016d,e);
  
  2. Stochastic models (Kapranova et al., 2016a,b, 2017, 2018a,b; Kapranova, 2018; Kapranova A. B. et al., 2019; Kapranova and Miadonye, 2019) for the process of bubble formation in the initial stage of hydrodynamic cavitation, the results of which are in satisfactory agreement (Kapranova and Miadonye, 2019) with the experimental data (Lebedev et al., 2017a,b) and justify the possibility of reducing the cavitation intensity in the node "separator-external locking shell."

- The proposed engineering methodology for calculating the main structural parameters of the node "separator-external locking shell" uses two approaches:
  
  1. Application of the Pi-Buckingham theorem (Buckingham, 1915; Misic et al., 2010) in solving the problem of scaling and lowering the number of constant parameters describing the process under study, within the framework of the well-known classical algorithm for choosing the type of control device (Arzumanov, 1971, 1985) based on the experimental relationships between the main process indicators (blocks 2 and 6, expressions (12) and (30), section Description of the Work Flowchart of the Engineering Methodology for Calculating the Parameters of These System of the Separator-External Locking Shell), as well as an empirical analysis of the conditions for attaining critical values of hydrodynamic similarity criteria: a) the Reynolds number (block 6, expression (28), section Description of the Work Flowchart of the Engineering Methodology for Calculating the Parameters of These System of the Separator-External Locking Shell); b) the cavitation coefficient as a doubled Euler number (Knapp et al., 1970; Franc and Michel, 2005; Xu et al., 2015; Kapranova et al., 2016e) (blocks 18 and 20, section Description of the Work Flowchart of the Engineering Methodology for Calculating the Parameters of These System of the Separator-External Locking Shell); (2) Using for calculating the set of sought-for structural parameters \( q^* = \{ q^*_k = const \}, k = 1, 5 \) functional dependencies obtained from models (Kapranova et al., 2016a,b, 2017, 2018a,b; Kapranova, 2018; Kapranova and Miadonye, 2019) and reflecting the conditions for the minimum size of the cavitation bubbles formed (block 17, expression (48), section Description of the Work Flowchart of the Engineering Methodology for Calculating the Parameters of These System of the Separator-External Locking Shell), energy parameters of the cavitation bubble system (blocks 14 and 15, expressions (38) and (42), section Description of the Work Flowchart of the Engineering Methodology for Calculating the Parameters of These System of the Separator-External Locking Shell), etc.

- When assessing the impact of the design parameters of the separator-external locking shell assembly on the nature of cavitation bubble formation, a comparative analysis (section The Influence of a Set of Design Parameters From the Rational Ranges of Their Change for the Node "Separator-Locking Shell" on the Size of Cavitation Bubbles) of the application of parameters from rational (Kapranova et al., 2020 according to the present methodology) and irrational (Kapranova A. B. et al., 2019) ranges of their change which showed that when using the results of Kapranova et al. (2020), there is a tendency to reduce the value between the ensemble average diameter value \( D_b \) by 1.95 times, while the transition from a mode from 20% for the degree of the opening of the separator to 80% for the opening of it’s throttle openings and the last operation is accompanied by an increase in the value of the conditional throughput of the \( K_{np} \) valve by 10.7 times.

Let us briefly dwell on the main directions of further improvement of the proposed engineering methodology for calculating the parameters of the separator-external locking shell unit, as an object of research of various nature (hydrodynamic, vibro-acoustic, managerial, etc.) that go beyond the scope of the tasks posed in this work. As already noted in section Methods, the relative error of theoretical calculations (Kapranova, 2018; Kapranova et al., 2018b; Kapranova and Miadonye, 2019) in comparison with experimental data (Lebedev et al., 2017a,b) in estimating the distribution of bubbles by the degree of opening of the axial valve with an external locking shell did not exceed 13% according to Kapranova and Miadonye (2019). This fact is reflected in the results of applying the engineering methodology described in section Results and Discussion, due to the use of...
the results of stochastic models (Kapranova, 2018; Kapranova et al., 2018b; Kapranova A. B. et al., 2019; Kapranova and Miadonye, 2019) for the process of bubble formation in the initial stage of hydrodynamic cavitation. However, these models do not take into account the consequences of the evolution of the cavitation phenomenon in the flow part of the valve, for example, the possible process of combining bubbles, the growth of their diameters and subsequent collapse. The emphasis in the proposed models and the corresponding engineering methodology for calculating the design parameters of the designed unit “separator-external locking shell” is made on the possibility of preventing an increase in the intensity of formation of cavities in the flow part of the regulating device already at the initial stage of the occurrence of cavitation. In addition, there are a number of difficulties that a designer may encounter in practice when implementing the described methodology. Additionally, it should be investigated: the conditions for reducing noise effects during the implementation of high-speed flow regimes of the working medium, and, therefore, vibro-acoustic characteristics; force factors in the movable elements of the device in order to calculate the hydrodynamic balance of the control valve; quality issues of the process of managing the static and dynamic characteristics of this unit, etc.

CONCLUSIONS

An analytical method has been developed for calculating the effective ranges of the structural parameters of the locking-regulating system “perforated separator—external locking cylinder-conical shell” based on the proposed stochastic models of bubble formation at the initial stage of hydrodynamic cavitation. In particular, in addition to the gyrodynamic similarity criteria, the following were used: differential distribution functions of the bubble distribution density at the initial stage of hydrodynamic cavitation in two phase variables—the conditional diameter of the cavitation bubble (Kapranova et al., 2018a) and the degree of valve opening (Kapranova and Miadonye, 2019). In addition, the proposed block diagram of the calculation of the node “separator-external locking shell” uses estimated analytical expressions: for the value of the coefficient of hydraulic resistance (Kapranova et al., 2018); for the average ensemble diameter of the cavitation bubble from the indicated works (Kapranova et al., 2016c); for the critical value of the Reynolds criterion depending on the desired design parameters (Kapranova, 2018).

When studying the influence of a set of design parameters for the “separator-external locking shell” assembly from certain rational ranges of their change, a tendency is found to reduce the ensemble average value of the diameter of the cavitation bubble by almost 2 times compared with the values of the parameters from irrational limits. It is shown that for these comparative cases, a change in the degree of opening of the throttle holes of the separator from 20 to 80% is able to change the valve throughput by more than 10 times.

The proposed methodology for the engineering calculation of the design parameters of an axial valve with an external location of the locking body is of interest to designers of control valves in the chemical and oil refining industries, and can be expanded when designing axial valves of other structures on a theoretical basis using a stochastic approach (Kapranova et al., 2019a).

DATA AVAILABILITY STATEMENT

All datasets generated for this study are included in the article/supplementary material.

AUTHOR CONTRIBUTIONS

All authors listed have made a substantial, direct and intellectual contribution to the work, and approved it for publication.

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**Conflict of Interest:** SN, AM, and DV were employed by the company JSC Regulator (Yaroslavl, Russia).

The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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