In this study, we explored the possibility of developing non-invasive biomarkers for patients with type 1 diabetes (T1D) by quantifying the directional couplings between the cardiac, vascular, and respiratory systems, treating them as interconnected nodes in a network configuration. Towards this goal, we employed a linear directional connectivity measure, the directed transfer function (DTF), estimated by a linear multivariate autoregressive modelling of ECG, respiratory and skin perfusion signals, and a nonlinear method, the dynamical Bayesian inference (DBI) analysis of bivariate phase interactions. The physiological data were recorded concurrently for a relatively short time period (5 min) from 10 healthy control subjects and 10 T1D patients. We found that, in both control and T1D subjects, breathing had greater influence on the heart and perfusion with respect to the opposite coupling direction and that, by both employed methods of analysis, the causal influence of breathing on the heart was significantly decreased ($p < 0.05$) in T1D patients compared to the control group. These preliminary results, although obtained from a limited number of subjects, provide a strong indication for the usefulness of a network-based multi-modal analysis for the development of biomarkers of T1D-related complications from short-duration data, as well as their potential in the exploration of the pathophysiological mechanisms that underlie this devastating and very widespread disease.

**Keywords:** directional connectivity, type 1 diabetes (T1D), dynamical Bayesian inference, directed transfer function (DTF), cardio-respiratory system

**INTRODUCTION**

Type 1 diabetes (T1D) is a chronic condition affecting roughly 5% of the world’s diabetic population (Ogurtsova et al., 2017), which is estimated to reach 642 million (95% CI: 521–829 million) by 2040 (it was 151 million in 2000 (Wild et al., 2004)) with dramatic social and financial implications. T1D is associated with pathogenetic mechanisms that lead to the apoptosis of pancreatic beta cells and, thus, to an inadequate production of the insulin hormone. There is no currently available cure for T1D, and its clinical care is focused primarily on the normalization of blood glucose levels for averting the onset of long-term complications including cardiovascular disease and renal failure. The treatment of diabetic-related chronic complications accounts for a considerable percentage [about 80% in the...
United Kingdom (Ogurtsova et al., 2017)] of the total medical costs of diabetes mellitus. Studies show that timing of medical intervention is key to reducing effects of comorbidities of T1D, with earlier interventions resulting in lower disease impact (Doria et al., 2012). Thus, there would be benefits to patients and healthcare systems alike from development of novel diagnostic techniques for early and non-invasive detection of T1D-related complications. Such diagnostic regimes could also have implications in outpatient monitoring and disease progression assessment.

The complex function of the cardiovascular system is realized by the synergistic activity of self-sustained cardiac, respiratory, and vascular oscillators (Ticcinelli et al., 2017), which is deemed to convey the necessary adaptability to sudden variations in the metabolic requirements of the organism or to changing environmental conditions (Penzel et al., 2017). There is a wide variety of clinically available devices for non-invasively monitoring the physiological systems that may be impacted by the progression of T1D. Such systems generate oscillatory modes that span a wide range of characteristic time scales, which can be isolated and separately characterized by means of established time-frequency representation (TFR) techniques (Clemson et al., 2016). In this regard, the wavelet transform (WT) analysis of laser Doppler flowmetry (LDF) signals of microvascular perfusion (Stefanovska et al., 1999) has contributed to the identification of myogenic (Aalkjaer et al., 2011), neurogenic (Söderström et al., 2003) and endothelial (Kvandal et al., 2006) frequency ranges in the microcirculatory vasomotion, in addition to the ones of the extrinsic cardiac and respiratory components (Stefanovska and Hozic, 2000) transmitted to the distal microvascular beds (Table 1). This, in turn, has enabled the non-invasive assessment of the underlying vasomotor mechanisms in pathological states.

Furthermore, the wavelet cross-spectrum (Clemson et al., 2016) and the phase coherence of bivariate data, (Sheppard et al., 2012; Tankanag et al., 2014; Perrella et al., 2018), along with statistical properties translated from information theory [e.g., Granger causality (Granger, 1969) and transfer entropy (Vejmelka and Palus, 2008; Sabesan et al., 2009)], have been used to gain insights into the presence of significant relations between oscillatory sources, and to determine the existence of a mutual physiological coordination, e.g., the well-known synchronous modulation of the heartbeat period by the breathing rhythm, produced at the respiratory centers located within the medulla oblongata and pons of the brainstem (Eckberg, 2003). However, beyond the effects manifested in the oscillators’ phase dynamics, the fundamental functional mechanisms underlying these interactions can be probed via more sophisticated techniques, able to provide information about the directional strength of the coupling and hence about the causality of the interaction (Rosenblum and Pikovsky, 2001; Palus and Stefanovska, 2003; Faes et al., 2004). Since the cardiovascular system must handle time-varying conditions, the employed methods should be capable of capturing non-stationary functional couplings. The dynamical Bayesian inference (DBI) technique, more recently introduced by Stankovski et al. (2012), seeks to account for such non-stationarities. In DBI, the cardiovascular system is modelled as a network of phase oscillators coupled by time-dependent functions, which are identified dynamically through a Bayesian estimation framework within subsequent time windows of the oscillators’ phase time series. Several researchers have employed DBI to investigate potential changes in the direct and indirect coupling between the cardiac, respiratory and vasomotor activities; their studies have detected a reduction in the respiratory sinus arrhythmia with ageing (Shiogai et al., 2010; Iatsenko et al., 2013; Stankovski et al., 2014; Ticcinelli et al., 2015; Ticcinelli et al., 2017), and a weakening of the coupling between the microvascular myogenic vasomotion and the central cardiac and respiratory oscillations in the elderly population and in primary hypertension (Ticcinelli et al., 2017). Since metabolic diseases, such as obesity and diabetes, have been recognized as models of accelerated ageing, the aforementioned alterations may also be present in subjects diagnosed with T1D.

Non-stationary metrics of time-frequency activity could elucidate stochastic coupling but require an adequate number of data points over stationary windows for inferences to be statistically significant. Linearly modelling the data may provide a valuable alternative. Multivariate autoregressive (MVAR) models have been used for describing interactions between time series originating from different nodes within a network (Baccalá et al., 2007; Vlachos et al., 2017). In detail, MVAR-based parametric techniques can be utilized to elucidate inter-node connections via coherence-based measures of implicit causality. One such measure is the directed transfer function (DTF), a frequency-domain descriptor of directed network connectivity with fundamental implications from Granger causality (Baccalá et al., 2007). DTF measures cascaded direct and indirect interactions, emphasizes source-based outflow and has been employed in several neuroscience applications (Kamiński et al., 2001; Blinowska et al., 2013; Kamiński and Blinowska, 2014;

| Oscillation       | Nominal range (Hz) |
|-------------------|---------------------|
| Cardiac           | (0.6, 2.0)          |
| Respiratory       | (0.145, 0.6)        |
| Myogenic          | (0.052, 0.145)      |
| Sympathetic       | (0.021, 0.052)      |
| Endothelial (NO-dependent) | (0.006, 0.021) |
| Endothelial (NO-independent) | (0.005, 0.0095) |

| Characteristics                  | Control | T1D  | p-value |
|----------------------------------|---------|------|---------|
| Gender (M/F)                     | 7/3     | 5/5  | 0.361*  |
| Age (years)                      | 26.7 ± 1.5 | 29.7 ± 13.3 | 1.000** |
| Smokers (Y/N)                    | 1/9     | 4/6  | 0.121*  |
| Heart rate (bpm)                 | 70.7 ± 7.2 | 74.1 ± 9.5 | 0.406*  |
| Breathing rate (Hz)              | 0.25 ± 0.06 | 0.28 ± 0.03 | 0.146*  |
| LDF cardiac power (%)            | 90.6 ± 6.6 | 91.7 ± 7.8 | 0.450*  |
| T1D duration (years)             | -       | 13.8 ± 10.0 | -      |
| HbA1c (%)                        | -       | 7.5 ± 1.1  | -      |

* via Pearson’s χ² test. ** via Mann-Whitney U test.
DTF and other MVAR-based measures of directional connectivity may also be applied to the evaluation of the directional coupling between the cardiac, respiratory, and peripheral blood flow systems. The utility of these measures in neuro-cardiorespiratory network interactions has been shown lately in animal studies of sudden unexpected death in epilepsy (SUDEP), a condition that involves potential failure of central control units of cardiac and respiratory behavior (Hutson et al., 2020).

Employing directed connectivity measures to quantify the inter-modulation of the biological oscillations originating from separate but interconnected systems could have valuable diagnostic potential for assessing the deterioration of the cardiovascular and respiratory function in prevalent high-risk conditions such as T1D. According to the results of a recent review article (Klein et al., 2010), adult subjects diagnosed with type 2 diabetes are characterized by reduced respiratory parameters, which appear to be inversely related to blood glucose levels and the time since the initial diagnosis. This review has linked chronic hyperglycemia and inflammation, autonomic neuropathy, microangiopathy of the pulmonary arterioles, and stiffening of the lung parenchyma to the possible biological mechanisms underlying the lung function.

FIGURE 1 | Experimental recording setup.

FIGURE 2 | Example of (A) ECG, (B) breathing and (C) LDF perfusion signals recorded from a young control subject.
perfusion signals. An example of the raw signals acquired from a young control individual is shown in Figure 2.

The mean breathing rate of all subjects was inside the nominal physiological range, that is (0.145, 0.6) Hz (Table 1). Furthermore, LDF perfusion signals recorded from the pathological group did not exhibit a significantly different ($p = 0.450$) power within the nominal frequency range of the cardiac rhythm (0.6, 2) Hz. However, T1D subjects included a larger proportion of smokers and were on average older than the control subjects. Nevertheless, these differences did not reach statistical significance according to Pearson’s $\chi^2$ and Wilcoxon rank-sum tests, respectively.

**Dynamical Bayesian Inference**

The functional physiological interaction between cardiac and respiratory processes was investigated by means of the dynamical Bayesian inference (DBI) technique (Duggento et al., 2012; Stankovski et al., 2012). This method regards the cardio-respiratory system as a network of coupled self-sustained nonlinear phase oscillators and uses a Bayesian inference scheme to dynamically estimate their time-evolving coupling strength and causality (i.e., the direction of interactions). Myogenic, sympathetic, and endothelial microvascular oscillations (Table 1) were not considered in the present study, due to the insufficient duration of the recorded signals. A comprehensive description of the approach can be found elsewhere (Duggento et al., 2012; Stankovski et al., 2012; Iatsenko et al., 2013; Clemson et al., 2016; Ticcini et al., 2017). Briefly, in DBI, the phase dynamics of two interacting oscillatory processes $p_1$ and $p_2$ is modelled as follows:

$$\dot{\phi}_1(t) = \omega_1(t) + d_1(\phi_2, t) + k_1(\phi_1, \phi_2, t) + \epsilon_1(t)$$

(1)

where $\omega_1(\cdot)$ is the natural frequency of the first oscillator, $d_1(\cdot)$ and $k_1(\cdot)$ are the coupling functions that describe the direct and indirect driving of the second oscillator (with the acceleration/deceleration of the first oscillator’s phase $\phi_1$ depending on the second’s $\phi_2$), whereas the stochastic term, $\epsilon(\cdot)$, represents the noise (usually assumed to be Gaussian and white (Stankovski et al., 2012)). Since the above coupling functions are hypothesized to be $2\pi$-periodic, the right-hand side of Eq. 1 can be decomposed into a linear combination of Fourier basis functions $\Phi_n = \exp[i(n_1\phi_1 + n_2\phi_2)]:$
\[ \phi_1(t) = \sum_{n=-N}^{N} c_{1,n} \cdot \Phi_1,0(\phi_1, \phi_2) + \varepsilon_1(t) \]  

(2)

where \( N \) is the order of the expansion and \( \Phi_{1,0} = 1 \) (where \( i = 1, 2 \)). In general, the DBI technique sequentially applies the Bayesian theorem to adjacent time windows of the oscillators' instantaneous phases, \( \phi_i(t) \), in order to infer the bank of time-varying parameters \( c_{i,n} \) characterizing the functional interaction between the underlying physiological processes, and the noise term, \( \varepsilon_i \). The inferred \( c_{i,n} \) values are then used to estimate a dynamic index of directional coupling strength and directionality of influence. In the present study, DBI analysis was based on the related Matlab toolbox developed by the research group on Nonlinear and Biomedical Physics at Lancaster University (http://www.physics.lancs.ac.uk/research/nbmpysics/diats/tfr/).

In detail, DBI analysis usually requires the extraction of the instantaneous frequency of the oscillations of interest, in order to track their characteristic time-dependent phase \( \phi_i(t) \). In this regard, an adaptive parametric ridge reconstruction scheme (Iatsenko et al., 2016) was applied to the time-frequency representation (TFR) of the acquired signals in order to isolate the breathing and cardiac oscillatory components. In the present study, the cardiac component was isolated from both the ECG and the LDF signals of cutaneous perfusion. The adjustable parameters of the algorithm, which respectively tune the tolerance to deviations from the component’s mean rate of frequency change and mean frequency, were set to their default value of 1. The wavelet transform (WT) was adopted as TFR technique because of its logarithmic frequency resolution (Stefanovska et al., 1999); specifically, a Morlet wavelet with central frequency \( f_0 = 1 \) was chosen as the mother function:

\[ y_m(t) = \frac{1}{\sqrt{2\pi}} \left( e^{i2\pi f_0 t} - e^{-\frac{i2\pi f_0^2}{2}} \right) e^{-t^2/2} \]  

(3)

Prior to the application of the WT, signals were downsamplled to 50 Hz, detrended by means of a third order polynomial fit, and band-passed inside the cardiac and respiratory frequency
TABLE 3 | Median coupling strength values obtained from 100 inter-subject surrogates.

| Interaction | DBI connectivity | Median surrogates (Nw = 2,300) |
|-------------|------------------|--------------------------------|
| Lungs ↔ Pulse | $s_{pulse→bre}$ | 0.08                           |
| Lungs ↔ Heart | $s_{ECG→pulse}$ | 0.24                           |
| Heart ↔ Pulse | $s_{pulse→ECG}$ | 0.09                           |
| Heart ↔ Lungs | $s_{ECG→bre}$ | 0.19                           |
| Heart ↔ Lungs | $s_{pulse→bre}$ | 0.28                           |
| Heart ↔ Lungs | $s_{ECG→pulse}$ | 0.25                           |

intervals listed in Table 1, to remove the influence of components lying outside the physiological range of interest. The discretization of the frequency domain was performed with a density of 128 voices/octave, which enabled the extraction of smooth ridge curves. DBI was then applied to consecutive overlapping windows of the original time series, with an overlap factor of 50%. The window width was set so as to include approximately five cycles of the slowest oscillatory component for inference of the coupling parameters $c_{ij,n}$, as reported in (Iatsenko et al., 2015; Clemson et al., 2016). For the analysis of cardio-respiratory interactions, this resulted in the adoption of 23 overlapping windows of 25 s. Thus, the lowest frequency we could theoretically observe was $1/25$ s = 0.04 Hz. The characteristic time-frequency ridges extracted from the signals in Figure 2 are shown in Figure 3.

As done by Iatsenko et al. (2013) and Ticcinelli et al. (2017), a Fourier decomposition up to the second order (i.e., $N = 2$) was chosen for the phase dynamics model expressed in Eq. 1. Moreover, the propagation constant $p_{w}$, that weights the diffusion of information between consecutive data windows $w$ (Stankovski et al., 2012), was set to an arbitrary value of 0.2. Iatsenko et al. (2013) have nonetheless reported that this internal parameter of the DBI algorithm does not significantly affect the outcome of the Bayesian inference. The Euclidean norm of the coupling parameters $c_{ij,n}$ estimated within each data window $w$ was finally used to quantify the overall influence (including direct and indirect couplings) of the phase of the second oscillator on the first one’s, and vice versa, yielding the following directional coupling strength signals:

$$s_{1→2}(w) = \sqrt{\sum_{n=1}^{N}(c_{1,n}(w))^2}$$

$$s_{2→1}(w) = \sqrt{\sum_{n=1}^{N}(c_{2,n}(w))^2}$$

where $w$ indicates the dependence of the coupling coefficients on the particular time window.

Furthermore, a directionality index $d_{1,2}$ ($d_{1,2} \in [-1, +1]$) was estimated from each window $w$, in order to quantify the dynamic asymmetry of the bi-directional interaction:

$$d_{1,2}(w) = \frac{s_{1→2}(w) - s_{2→1}(w)}{s_{1→2}(w) + s_{2→1}(w)}$$

This index, proposed by Rosenblum and Pikovsky (2001) has been used in the recent literature for detecting the predominant direction of influence between the cardiac and respiratory oscillators (Stankovski et al., 2012; Iatsenko, et al., 2013; Ticcinelli, et al., 2017). Namely, if $d_{1,2} \in [0, +1]$, then the first oscillator drives the second more than the other way around; conversely, if $d_{1,2} \in [-1, 0)$, the second drives the first one. However, as reported in (Duggento et al., 2012), directional coupling strengths $s_{i→j}(w)$ obtained via DBI represent an overall estimate of the combined phase relationships between the analyzed time series. Thus, spurious non-zero values can be inferred even when no functional interaction exists between the underlying oscillatory processes. This is why the reliability of $s_{i→j}(w)$ should be ascertained by surrogate testing, i.e., rejecting directional coupling strengths below a specified acceptance threshold estimated from an adequately large set of surrogate interactions. In this regard, we adopted the inter-subject surrogate approach followed by Toledo et al. (2002) and Ticcinelli et al. (2017) validating our coupling strength estimates against the median value obtained from 100 unique combinations of randomly selected inter-group signals and subjects. Each of the 100 surrogate datasets was composed of mutually independent time series recorded from different individuals (e.g., ECG from control subject A, breathing from T1D patient B, LDF perfusion from control C). This technique allowed us to exclude from further consideration any directional couplings whose strength was equivalent to the one which might have arisen from chance or bias.

**Directed Transfer Function**

Multivariate autoregressive (MVAR) modelling of the data within short-time segments, each data window aligned in time with concurrent ones from more than one time series, is recommended for network connectivity analysis assuming that these signals are recorded from different parts of a multi-dimensional, linear and wide-sense stationary system. For each window, the estimated array of MVAR model coefficients can then be further analyzed in the frequency domain and, depending on different types of normalization utilized, provides frequency-specific measures of directional functional connectivity between the nodes of the assumed network configuration of the system (Baccalà et al., 2007). We have successfully employed such measures in network analyses of intracranial EEG (iEEG) (Vlachos et al., 2017; Adkinson et al., 2018), and magnetoencephalographic (MEG) recordings (Krishnan et al., 2015) from patients with focal epilepsy for localization of their epileptogenic focus, as well as the assessment of the dynamics of brain’s network connections en route to a life-threatening neurological event, status epilepticus (T. N. Hutson et al., 2018). In the current study we fitted a MVAR model to each of 60-s consecutive non-overlapping data segments from the three recorded signals (ECG, breathing, perfusion) over 5 min. By using a 60-s time window, our frequency resolution is $1/60 = 0.017$ Hz = 0.05 Hz/3, and thus the lowest frequency we can deal with moving the analysis in the frequency domain is three times less than the 0.05 Hz, the lowest frequency in the frequency band of (0.05, 2) Hz we are interested in here. Thus, the MVAR model was of dimension $D = 3$ [i.e., the data to be fitted were placed in three-dimensional column vectors $X(t)$], and of
order $M = 7$ per subject. Also, the window length of 60 s (15,000 data points x three channels = 45,000 data points) is enough for a confident estimation of the $7 \times 3 \times 3 = 63$ MVAR parameters as we are using more than 100 times as many data points as we have parameters to fit.

For each set of three 60-s running windows extracted at the same time from all three signals, the model linearly fits the data in the column vectors $X(t)$ as follows:

$$X(t) = \sum_{\tau=1}^{M} A(\tau)X(t-\tau) + E(t) \quad (7)$$

where the time index $t$ is from 1 to $N$, with $N$ being the number of data points per time series within a time window ($N = 15,000$), $M$ is the order of the model ($M = 7$), and $\tau$ is increasing in steps of the time delay between samples (we used $\tau = 1$, that is, in time units, equal to the sampling period $1/(250 \text{ Hz}) = 4 \text{ ms}$). Matrices $A(\tau)$ contain the model’s coefficients, whereas the fitting error values are the components of the vector $E$ (in the ideal MVAR model fit, $E$ is multivariate Gaussian white noise). The coefficients of the MVAR model were estimated via the Vieira-Morf partial correlation method. Taking the discrete Fourier Transform of both sides of Eq. 7 and rearranging, we have: $[I - \sum_{\tau=1}^{M} A(\tau)e^{-i2\pi f\tau}] \cdot X(f) = E(f)$, where $I$ is the unitary matrix. Then, by defining:

$$B(f) = \begin{cases} 
I - \sum_{\tau=1}^{P} A_{jj}(\tau)e^{-i2\pi f\tau}, & \text{for } i = j \\
-\sum_{\tau=1}^{P} A_{ij}(\tau)e^{-i2\pi f\tau}, & \text{for } i \neq j 
\end{cases} \quad (8)$$

where $i = \sqrt{-1}$ in the exponents of Eq. 8, the directed transfer function (DTF) can be derived by utilizing the transfer matrix, $H(f)$, defined as:

$$H(f) = B^{-1}(f) \quad (9)$$

Specifically, DTF is estimated via the following equation:

$$DTF_{j \rightarrow i}(f) = \frac{|H_{ij}(f)|^2}{\sum_{k=1}^{D}|H_{ik}(f)|^2} \quad (10)$$

The statistical significance of the DTF values of each interaction derived from each 60-s window was determined. The statistical criteria for inferring the statistical significance and confidence interval of the derived frequency-domain Granger causality-based connectivity measures are recent and have been discussed by a small number of researchers. In this study, we have followed an asymptotic analysis for evaluation of the connectivity measures from the MVAR modelling of our data (Baccalà et al., 1997; Baccalà et al., 2016). In detail, the significance of the connectivity measures $DTF_{j \rightarrow i}(f)$ at a specific frequency $f$ between two nodes $i$ and $j$ was tested according to the following null hypothesis:

$$H_0: \ |DTF_{j \rightarrow i}(f)|^2 = 0 \quad \forall i, j \in \{1, \ldots, D\} \quad (11)$$

Rejecting $H_0$ at a specified significance level (typically $\alpha = 0.05$) also required to reject non-statistically significant DTF values. Confidence intervals for the existing connections were estimated by determining the asymptotic distribution of DTF according to (Toppi et al., 2016). Only the thus identified statistically significant DTF values (ssDTF) were further analyzed in this study. Analogously to the DBI...
analysis, an index of directionality was finally obtained from the ssDTF estimates as follows:
\[ d_{ij}(f) = \frac{ssDTF_{i\rightarrow j}(f) - ssDTF_{j\rightarrow i}(f)}{ssDTF_{i\rightarrow j}(f) + ssDTF_{j\rightarrow i}(f)} \]  

RESULTS

Dynamical Bayesian Inference

Figure 4 shows sample coupling strength signals of the time-evolving pairwise interactions among peripheral pulse, respiratory and ECG signals, estimated using DBI in a control subject and a T1D patient. Directional coupling strength estimates below the corresponding median values of the surrogates reported in Table 3 (100 surrogate subjects, for a total of \( N_w = 2,300 \) windows), were rejected. Also, only those windows for which both directional coupling strengths per paired interaction were found to be statistically significant according to the above rule were further considered in the statistical analysis of the directionality index, \( d_{ij} \). The overall results of the DBI analysis of the control and pathological groups including their statistical comparison (\( p \)-values) are shown in Figure 5 and summarized in Table 4. Statistically significant differences

| Interaction | DBI connectivity | Median (controls) | Median (T1D) | \( p \)-value \( H_{1a} \) | \( p \)-value \( H_{1b} \) |
|-------------|------------------|------------------|--------------|-------------------|-------------------|
| Lungs → Pulse | \( s_{pulse\rightarrow bre} \) | 0.120 | 0.134 | 0.948 | 0.051 |
| | \( s_{ECG\rightarrow pulse} \) | 0.361 | 0.363 | 0.326 | 0.674 |
| | \( d_{bre, pulse} \) | 0.539 | 0.455 | 0.011* | 0.990 |
| Lungs → Heart | \( s_{ECG\rightarrow bre} \) | 0.127 | 0.140 | 0.887 | 0.113 |
| | \( s_{bre\rightarrow ECG} \) | 0.360 | 0.314 | <0.001* | 1.000 |
| | \( d_{bre, ECG} \) | 0.503 | 0.396 | <0.001* | 0.999 |
| Heart → Pulse | \( d_{pulse\rightarrow ECG} \) | 59.21 | 37.51 | <0.001* | 0.999 |
| | \( s_{ECG\rightarrow pulse} \) | 82.86 | 33.44 | <0.001* | 1.000 |
| | \( d_{ECG, pulse} \) | 0.013 | 0.042 | 0.556 | 0.445 |

*Statistically significant at \( \alpha = 0.05 \) level (one-tailed Wilcoxon rank-sum test).
between the two groups were detected by means of one-tailed Wilcoxon rank-sum tests for independent samples.

Lungs–Heart interaction. Compared to controls, T1D patients exhibited a significant reduction in the directionality index \(d_{\text{bre, ECG}}\) \((p < 0.001)\), which reflects a lowered asymmetry of the cardiorespiratory interaction in the pathological group. This was due to a weakened influence of the breathing activity on the cardiac rhythm, as expressed by the statistically significant decrease in the directional coupling strength \(s_{\text{bre--ECG}}\) \((p < 0.001); \text{Table 4, row 4}\). Conversely, the directional coupling from the heart to the lungs was not significantly different between the two groups (\text{Table 4, row 5}\).

Lungs–Pulse interaction. T1D patients also exhibited a significant decrease in the \(d_{\text{bre, pulse}}\) index \((p = 0.011)\), which indicates a higher symmetry of the interaction between the breathing activity and the cardiac oscillatory mode of the LDF signals. However, in this case, none of the corresponding directional coupling strengths was significantly different between the compared subjects (\text{Table 4, rows 1 and 2}\).

Heart–Pulse interaction. With respect to the healthy group, T1D patients were characterized by significantly lowered directional coupling strengths, \(s_{\text{pulse--ECG}}\) \((p < 0.001); \text{Table 4, row 7}\) and \(s_{\text{ECG--pulse}}\) \((p < 0.001); \text{Table 4, row 8}\). However, no statistically significant difference emerged in the overall directionality of influence, as expressed by the \(d_{\text{ECG, pulse}}\) index across the control and pathological groups (\text{Table 4, row 9}\).

### Directed Transfer Function

The statistically significant DTF values (ssDTF) of directional connectivity estimated per interaction from MVAR modelling (six directional interactions between the three recorded signals) were aggregated over all windows (60-s non-overlapping data segments) and subjects within the same group (control or T1D) and averaged over the physiologically relevant frequency band \((0.05, 2)\) Hz. The median and quartiles of the ssDTF values obtained from the control and T1D groups are shown in \text{Figure 6}\. It is relevant to highlight that MVAR modelling evaluates signals across identical frequencies over the entire physiological range of interest, in contrast to DBI which is based on the extraction of the specific time-varying frequency component of the cardiac pulsatility, within an effectively tighter range. Therefore, in this section interactions involving LDF signals are denoted as “perfusion”, rather than “pulse”. From \text{Figure 6}, we make the following statistically significant observations about the assessed directional interactions: “Perfusion→Breathing”, “Perfusion→ECG” and “ECG→Breathing” connectivity strengths are elevated in T1D subjects compared to controls. Conversely, the “Breathing→ECG” interaction in T1D is lower than the controls. It is also noteworthy that “Breathing→ECG” is significantly higher in connectivity than “ECG→Breathing” for both T1D and controls. Also, the “Perfusion→ECG” coupling is higher than “ECG→Perfusion” in both groups.

Statistically significant directional interactions \((p < 0.05)\) between the network nodes for each pair of recorded signals are reported in \text{Table 5} (columns 3 and 4) together with their directionality index \(d_{i,j}\). Inter-group comparisons were conducted via one-tailed Wilcoxon rank-sum statistical tests, whose \(p\)-values are also included in \text{Table 5} (last two columns).

Lungs–Heart interaction. In agreement with the results from the DBI method, DTF shows that T1D patients exhibit a statistically significant reduction \((p < 0.001)\) in the directional coupling strength from the lungs to the heart, as well as in the directionality index \(d_{\text{bre, ECG}}\) compared to controls. The latter is due to a statistically significant increase \((p < 0.001)\) in the directional strength \(ssDTF_{\text{bre--ECG}}\) observed in the pathological group, with a parallel significant decrease \((p < 0.001)\) in \(ssDTF_{\text{bre--ECG}}\) (\text{Table 5, rows 4–6}\).

Lungs–Perfusion interaction. Similarly to the DBI analysis, the DTF measures of connectivity showed a decrease in the \(d_{\text{bre, pulse}}\) index of T1D patients compared to the one estimated from the control group \((0.729 vs. 0.276)\), implying a lowered asymmetry of the interaction between breathing and LDF signals. However, this decrease was not as significant \((p = 0.084)\) as the one estimated via DBI \((p = 0.011)\). This outcome is due to the mixed results (decrease with \(p = 0.031\), and increase with \(p = 0.019\)) related to the directional coupling strengths \(ssDTF_{\text{bre--perf}}\) and \(ssDTF_{\text{perf--bre}}\) respectively (\text{Table 5, rows 1 and 2}\).

Heart–Perfusion interaction. T1D patients exhibited increased connectivity compared to the controls in both directions, with the difference in the “Perfusion→ECG” coupling reaching statistical significance \((p = 0.002)\) (\text{Table 5, rows 7 and 8}\). The above trends contributed to a diminished absolute value of the directionality index \(d_{\text{ECG, perf}}\) in the pathological group, which implies a more balanced interaction with respect to controls (\text{Table 5, row 9}\).

### Table 5

| Interaction | DTF connectivity | Median (controls) | Median (T1D) | \(p\)-value \(H_{1a}\) | \(p\)-value \(H_{1b}\) |
|-------------|------------------|------------------|--------------|----------------|------------------|
| Lungs ↔ Perfusion | \(ssDTF_{\text{bre}}\,\rightarrow\text{bre} \) | 0.027 | 0.074 | 0.982 | 0.019* |
| | \(ssDTF_{\text{bre}}\,\rightarrow\text{ECG} \) | 0.510 | 0.129 | 0.031* | 0.970 |
| | \(d_{\text{bre, perf}}\) | 0.729 | 0.276 | 0.084 | 0.918 |
| Lungs ↔ Heart | \(ssDTF_{\text{bre}}\,\rightarrow\text{bre} \) | 0.002 | 0.011 | 1.000 | <0.001* |
| | \(ssDTF_{\text{bre}}\,\rightarrow\text{ECG} \) | 0.897 | 0.634 | <0.001* | 1.000 |
| | \(d_{\text{bre, ECG}}\) | 0.992 | 0.964 | <0.001* | 1.000 |
| Heart ↔ Perfusion | \(ssDTF_{\text{bre}}\,\rightarrow\text{bre} \) | 0.055 | 0.121 | 0.998 | 0.002* |
| | \(ssDTF_{\text{ECG}}\,\rightarrow\text{bre} \) | 0.002 | 0.006 | 0.763 | 0.258 |
| | \(d_{\text{ECG, perf}}\) | -0.940 | -0.865 | 0.646 | 0.379 |

*Statistically significant at \(a = 0.05\) level (one-tailed Wilcoxon rank-sum test).
Finally, within each group, a few interesting features were also observed from the DTF results in relation to the difference in the strength of the directional couplings per interaction. In particular, in both control subjects and T1D patients, the median coupling strengths from the lungs to the heart and from the lungs to the microcirculation were considerably higher than in the opposite direction (the same outcome of the DBI analysis). However, the inter-group differences in the directional strengths between heart and microcirculation were contradictory with respect to the DBI analysis, which associated a higher level of bidirectional connectivity to the control group (Table 5, columns 3 and 4).

**DISCUSSION**

Towards the goal of developing reliable and non-invasive biomarkers for T1D, we employed both nonlinear (bivariate) and linear (multivariate) measures to assess possible impairments in the coupling strength and directionality of influence between three representative nodes of the cardiovascular and respiratory systems (heart, lungs, microcirculation) in patients diagnosed with T1D compared to control subjects. The two adopted methods can capture equivalent or different features in the communication between the nodes of a physiological network because of their different capabilities, that is: linearity (DTF) vs. nonlinearity (DBI) in the data; multivariate (DTF) vs. bivariate (DBI) data analysis; measure of connectivity between signals at the same frequency (DTF) vs. different frequencies (DBI). Employing these two techniques, we did identify impairments (by both or one of the approaches) in the functional directional interactions between heart, lungs, and microcirculation in T1D patients. In detail, an impairment was defined as a statistically significant difference ($p < 0.05$) in the directional coupling strengths between the respective nodes, compared to the homologous estimate obtained from the control group (i.e., rejection of the null hypothesis $H_0$).

Regarding the functional interactions between heart and lungs, DBI, the nonlinear framework, revealed a significantly reduced ($p < 0.001$) influence of the respiratory activity on the phase of the cardiac rhythm in the T1D group. A similar, statistically significant ($p < 0.001$) finding also emerged from the linear network analysis, using DTF. Moreover, the imbalance in the two communication channels from the lungs to the heart and vice versa, as captured by the directionality index, was also highly significantly different in both methods ($p < 0.001$). It is well known that the phase of the respiratory activity directly influences the action of the heart pump, as breathing-related changes in the intrathoracic volume alter the cardiac pre-load, thus affecting cardiac filling, post-load and other circulatory variables. Furthermore, respiration gates the timing of autonomic motoneuron firing (Eckberg, 2003), thus modulating the peripheral autonomic nervous system’s outflow to the heart, an indirect cardio-respiratory coupling occurring via neuronal control (Iatsenko et al., 2013; Kralemann et al., 2013).

Therefore, our finding of a reduced driving relationship of the lungs to the heart in T1D patients could be related to autonomic neuropathy, vascular degeneration or lung tissue stiffening, common co-morbidities associated with diabetes mellitus (Klein et al., 2010).

An analogous decrease of the influence of respiration on the microvascular perfusion in the T1D group compared to controls was observed by DTF analysis ($p = 0.031$) but could not be verified by DBI ($p > 0.05$). However, like for the lungs-heart interaction, the imbalance in the directional coupling strengths between lungs and microcirculation, as reflected by the directionality index, was significantly less ($p = 0.011$) in T1D than in controls as shown by DBI as well as by DTF, though without reaching a statistical significance level ($p = 0.084$). Also, regarding the DBI analysis of phase interactions, it is notable that control subjects exhibited similar statistics with respect to the evaluation of breathing and ECG signals. This result would be in line with previous findings by Jamšek and Stefanovska on the coupling information among cardiac and respiratory processes which propagates to the distal microvascular beds (Jamšek and Stefanovska, 2007), and can be characterized through the analysis of LDF signals recorded non-invasively from the skin.

In T1D subjects, the DBI analysis highlighted a significantly decreased communication in both directions between the ECG and the microvascular pulse signal extracted from LDF signals. This finding, however, could not be validated by DTF too. It is noteworthy that these directional interactions were associated with significantly higher coupling strength values (Table 4). This could be due to the way DBI evaluates causal relationships and what it can capture. In this case, DBI basically assesses the phase coupling between ECG and pulse signals that, although recorded at different anatomical locations, originate from the same source, representing the electrical and mechanical activities of the heart, respectively (Kralemann et al., 2013).

Finally, the estimated directional couplings from the lungs to the heart and microvasculature, via either the DBI or DTF methods, were considerably higher than the ones from the heart and vasculature towards the lungs, in both control subjects and T1D patients. Since this outcome was common in both groups, it cannot be used as a biomarker for T1D. However, it agrees with the findings of Palus and Stefanovska (2003), which have shown that the respiratory process drives the heart activity at all breathing frequencies, whether paced or spontaneous, and may shed more light on the involved physiological mechanisms en route to a better understanding of the cardio-respiratory system.

A potential limitation of this study is the availability and analysis of signals from only a small number of nodes (lungs, heart, microcirculation) in the network under investigation. Both DTF and DBI measure the global (direct and indirect) interactions between two nodes A and B, the indirect interactions from A to B or from B to A occurring through other node(s) C that we may not have access to in the network (Kamiński et al., 2001; Baccalá et al., 2016). In this regard, it is established that each respiratory cycle is tightly controlled by four separate control centers in the pons and medulla (Smith et al., 1991; Hilaire and Pásaro, 2003; Dampney, 2017), which cannot operate without central intervention from the brain, and direct feedback from the heart. Furthermore, central
autonomic neural control has a well-known role in the low- and high-frequency variability of the heart rate (Shaffer and Ginsberg, 2017). Thus, ignoring the brain (EEG) and investigating this complex neuro-cardio-respiratory network from only three nodes (lungs, heart, microcirculation) could have skewed the level of the estimated bivariate interactions in both T1D and control groups. However, the comparative statistical analysis of each measure across the two groups may take care of this skewness if it were in the same direction in both groups, per interaction.

In summary, we found that in both control and T1D subjects, breathing had greater influence on the heart and peripheral microvascular perfusion, compared to the opposite directional couplings and that, by both the employed methods of connectivity analysis, the causal influence of the respiratory activity on the heart was significantly decreased \((p < 0.05)\) in T1D patients compared to the control group. These preliminary results can be linked to established comorbidities of T1D and, although obtained from a limited number of subjects, provide a strong indication for the usefulness of a network-based multimodal analysis for the development of biomarkers from short-duration data, and for monitoring the disease and T1D-related complications over time, as well as its potential in the exploration of the pathophysiological mechanisms that underlie this devastating and very widespread disease.

DATA AVAILABILITY STATEMENT

The raw data supporting the conclusion of this article will be made available by the authors, without undue reservation.

REFERENCES

Aalkjaer, C., Boedtkjer, D., and Matchkov, V. (2011). Vasomotion - What Is Currently Thought? Acta Physiol. 202, 253–269. doi:10.1111/j.1748-1716.2011.02320.x
Adkinson, J. A., Karumuri, B., Hutson, T. N., Liu, R., Alamoudi, O., Vlachos, I., et al. (2018). Connectivity and Centrality Characteristics of the Epileptogenic Focus Using Directed Network Analysis. IEEE Trans. Neural Syst. Rehabil. Eng. 27 (1), 22–30. doi:10.1109/TNSRE.2018.2886211
Baccalá, L. A., de Brito, C. S., Takahashi, D. Y., and Sameshima, K. (1997). Unified Asymptotic Theory for All Partial Directed Coherence Forms. Philos. Trans. A. Math. Phys. Eng. Sci. 371, 20120158. doi:10.1098/rsta.2012.0158
Baccalá, L. A., Sameshima, K., and Takahashi, D. (2007). "Generalized Partial Directed Coherence," in 2007 15th International Conference on Digital Signal Processing, Cardiff, UK, 1–4 July 2007, 3, 163–166. doi:10.1109/icsp.2007.4288544
Baccalá, L. A., Takahashi, D. Y., and Sameshima, K. (2016). Directed Transfer Function: Unified Asymptotic Theory and Some of Its Implications. IEEE Trans. Biomed. Eng. 63 (12), 2450–2460. doi:10.1109/tbme.2016.2550199
Blinowska, K. J., Kamiński, M., Brzezicka, A., and Kamiński, J. (2013). Application of Directed Transfer Function and Network Formalism for the Assessment of Functional Connectivity in Working Memory Task. Philos. Trans. A. Math. Phys. Eng. Sci. 371, 20110614. doi:10.1098/rsta.2011.0614
Clemson, P., Lancaster, G., and Stefanovska, A. (2016). Reconstructing Time-Dependent Dynamics. Proc. IEEE 104 (2), 223–241. doi:10.1109/jproc.2015.2491262
Dampney, R. (2017). Central Mechanisms Regulating Coordinated Cardiovascular and Respiratory Function. Oxford Res. Encyclopedia Neurosci. 1, 1–27. doi:10.1093/acrefore/9780190264086.013.64

ETHICS STATEMENT

Ethical review and approval was not required for the study on human participants in accordance with the local legislation and institutional requirements. Written informed consent to participate in this study was provided by the participants’ legal guardian/next of kin.

AUTHOR CONTRIBUTIONS

MS collected and shared data with United States site, conceptualized and performed the dynamical Bayesian inference, in addition to compiling and preparing results for publication. TH conceptualized and performed the directed transfer function analysis in addition to compiling and preparing results for publication. LI gave input and expertise on signal processing and analysis, and assisted with full preparation and review of the manuscript. LB provided expertise on data, disease state, and analytical decisions in addition to preparation and review of the manuscript. All authors contributed to review and revision of results and final manuscript.

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Doria, A., Niewczas, M. A., and Fiorina, P. (2012). Can Existing Drugs Approved for Other Indications Retard Renal Function Decline in Patients with Type 1 Diabetes and Nephropathy? Semin. Nephrol. 32 (5), 437–444. doi:10.1016/j.smemph.2012.07.006
Duggento, A., Stankowski, T., McClintock, P. V., and Stefanovska, A. (2012). Dynamical Bayesian Inference of Time-Evolving Interactions: from a Pair of Coupled Oscillators to Networks of Oscillators. Phys. Rev. E Stat. Nonlin Soft Matter Phys. 86, 061126. doi:10.1103/PhysRevE.86.061126
Eckberg, D. L. (2003). The Human Respiratory Gate. J. Physiol. 548 (2), 339–352. doi:10.1113/jphysiol.2002.037192
Faes, L., Porta, A., Cucino, R., Cerutti, S., Antolini, R., and Nollo, G. (2004). Causal Transfer Function Analysis to Describe Closed Loop Interactions between Cardiovascular and Cardiorespiratory Variability Signals. Biol. Cybern. 90 (6), 390–399. doi:10.1007/s00422-004-0488-0
Granger, C. W. J. (1969). Investigating Causal Relations by Econometric Models and Cross-Spectral Methods. Econometrica 37 (3), 424–438. doi:10.2307/1912791
Hilaire, G., and Pásaro, R. (2003). Genesis and Control of the Respiratory Rhythm in Adult Mammals. News Physiol. Sci. 18, 23–28. doi:10.1152/nips.01402.2002
Hutson, T., Pizarro, D., Pati, S., and Iasemidis, L. D. (2018). Predictability and Resetting in a Case of Convulsive Status Epilepticus. Front. Neurol. 9, 172–178. doi:10.3389/fneur.2018.00172
Iatsenko, D., Bernjak, A., Stankowski, T., Shiogai, Y., Owen-Lynch, P. J., Clarkson, P. B., et al. (2013). Evolution of Cardiorespiratory Interactions with Age. Philos. Trans. A. Math. Phys. Eng. Sci. 371, 20110622. doi:10.1098/rsta.2011.0622
