Beam Management in 5G: A Stochastic Geometry Analysis
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Abstract—Beam management is central in the operation of beamformed wireless cellular systems such as 5G New Radio (NR) networks. Focusing the energy radiated to mobile terminals (MTs) by increasing the number of beams per cell increases signal power and decreases interference, and has hence the potential to bring major improvements on area spectral efficiency (ASE). This paper proposes a first system-level stochastic geometry model encompassing major aspects of the beam management problem: frequencies, antenna configurations, and propagation; physical layer, wireless links, and coding; network geometry, interference, and resource sharing; sensing, signaling, and mobility management. This model leads to a simple analytical expression for the effective rate that the typical user gets in this context. This in turn allows one to find the number of beams per cell and per MT that maximizes the effective ASE by offering the best tradeoff between beamforming gains and beam management operational overheads and costs, for a wide variety of 5G network scenarios including millimeter wave (mmWave) and sub-6 GHz. As part of the system-level analysis, we define and analyze several underlying new and fundamental performance metrics that are of independent interest. The numerical results discuss the effects of different systemic tradeoffs and performance optimizations of mmWave and sub-6 GHz 5G deployments.

Index Terms—5G NR, beam management, handover, interference, Poisson point process, stochastic geometry

I. INTRODUCTION

The ever-increasing demand in capacity for mobile communications necessitates new implementation approaches that can significantly boost data rates and the area spectral efficiency (ASE) of mobile networks. One key enabler considered in 5G [2] to face this demand is the use of the spectrum beyond the sub-6 GHz frequencies, known as millimeter wave (mmWave). More specifically, 5G is designed to make use of spectrum above 20 GHz, where bandwidth sizes of up to 400 MHz per carrier can be used to offer very high data rates (above 10 Gbps peak rates) and increase the network capacity [3]; nevertheless, the sub-6 GHz bands, with up to 100 MHz of bandwidth per carrier, are still needed to ensure wide area coverage and data rates up to a few Gbps [4].

One of the key difficulties faced by 5G operation on mmWave frequencies is their challenging propagation characteristics: they are subject to high path loss, penetration loss, and diffraction loss, and are thus limited to short distance links, typically of a few hundred meters. But what was once considered a limitation makes nowadays mmWave a suitable candidate for small cells deployments, which can be used for network densification and capacity boosting.

To overcome the propagation challenges at mmWave frequencies, steerable antenna arrays with a large number of antenna elements each can be used to create highly directional beams that concentrate the transmitted energy to achieve high gains and increase coverage. Also, mmWave communications must be designed to operate under mobility conditions, covering users in LOS (Line-of-Sight) and NLOS (Non-Line-of-Sight) at pedestrian and vehicular speeds. This can become quite challenging since operation at mmWave frequencies is highly sensitive to changes in the environment (e.g., moving of the hand/head, passing cars). Thus, any mmWave-based wireless access system relies on techniques such as adaptive beamforming, beam-tracking and fast beam-switching to always maintain the best selected beam that maximizes the performance even in the face of beam misalignment events due to intra-cell mobility and inter-cell handovers. Although more important for mmWave frequencies, beamforming techniques with directional narrow beams can also be used in sub-6 GHz frequencies to improve the network performance.

A. Motivation

The introduction of beamforming as a central feature in 5G New Radio (NR) requires a series of beam management procedures to ensure efficient operation. One of such procedures is the so-called beam selection (or, beam refinement). Here the mobile terminal (MT) monitors beamformed reference signals (RSs) periodically transmitted by the base station (BS) to identify and report to the BS the best serving BS beam. Such RSs can be either synchronization signal/physical broadcast channel blocks (SSBs), or channel state information reference signals (CSI-RSs). Another such procedure is the beam failure detection and recovery, where the MT monitors the radio link quality of the serving BS beam. If the quality of the radio link is repeatedly below a certain threshold, the BS triggers a procedure to quickly re-establish communication on neighboring beams.

Although beam management procedures are necessary for beamformed 5G NR operations, they also bring inherent costs
TABLE I: New Performance Metrics

| Performance Metric             | Formula | Interpretation of the Metric                                                                 |
|-------------------------------|---------|-----------------------------------------------------------------------------------------------|
| Probability of beam misalignment | (3) and (4) | The probability of beam misalignment between the beams of the BS and the MT due to the mobility of the MT between two consecutive beam measurement events |
| Intensity of geometry-based beam reselection | (17) | Frequency of geometry-based beam switching within a BS cell                                     |
| Geometry-based time-of-stay    | (19)    | Average time spent by the MT within the main lobe of a beam                                     |
| Effective intensity of beam reselection | (18)  | Frequency of beam reselections within a cell by taking into account the geometry and the system design. It determines the time overhead associated with beam reselection. |
| Effective time-of-stay         | (20)    | Average duration of time intervals during which the MT has selected any given serving BS beam, which is essential to, e.g., evaluate whether the MT will have enough time to perform MT beam refinement and link adaptation before data transmission |
| Probability of a beam switch  | (23)    | At a cell boundary, it is the probability that the MT has to switch panels/beams. This allows one to predict a no beam switching event, which can help reduce the number of beam measurements and the associated time overhead. |
| Time overheads                 | (21), (22), (24) | The time overheads are associated with the MT mobility and reference signal measurements in 5G that are necessary for inter-cell handovers and beam switching within the cell. The overheads determine the effective time available for data transmission. |

in terms of signaling and delay overheads. For instance, there should be one beamformed BS RS for each beam in the beamset for a proper beam management operation. Hence, increasing the beamset size increases the signaling overhead. Thus, the network planning for 5G NR deployments must take beam management into consideration. This requires the understanding of existing systemic effects and tradeoffs for any given MT mobility pattern, inter-site distance (inter-BS distance), and the number/width of the beams. For example, the adoption of a BS beamset containing a large number of narrow beams during the network planning phase improves the signal-to-interference-plus-noise ratio (SINR). But it may also lead to more frequent service interruption due to, e.g., beam switching delays (i.e., between the moment the BS RSs are measured and reported and the moment the BS decides to make the beam switch) and beam misalignment, which in the end may degrade the network performance. System-level simulations can be crucial to evaluate all such tradeoffs and determine the best combination of parameters for a given network deployment. But given the complex nature of beamforming and beam management procedures in 5G NR, such simulations can be very time-consuming and expensive. This paper proposes a mathematical framework that permits a system-level analysis of beam management in 5G, leads to insights into the associated tradeoffs, and has the potential to make beam management efficient. We believe that this mathematical framework will complement and help guide system-level simulations.

B. Contributions

1) We develop a first mathematical optimization framework for the beam management problem in 5G. Using the well-established tools from stochastic geometry [5]–[8], our proposed optimization yields the number of beams at the BS and the MT that maximizes the effective ASE of downlink transmissions to the directional MT.

2) The optimization permits a system-level analysis of 5G NR deployment based solely on a small set of input parameters. In particular, it takes into account the average speed of the MTs, mobility-induced beam misalignment, geometry-based beam selections during BS handovers and beam reselections within a cell, and time overheads associated with these beam (re)selections. For instance, given a mix of omnidirectional and directional MTs, a mix of MT speeds (pedestrians, bikes, and cars), a mix of geometries (some cells are bigger, other smaller, with the MTs either close or far from the serving BS), a mix of fading and blockages present in the network, our proposed optimization framework enables the identification of the number of beams that provides the best effective ASE, namely the best “sum rate” for MTs of all types in a large domain.

3) As part of the calculation of the effective ASE at the system level, we define and evaluate many new and fundamental performance metrics. These metrics are of independent interest and are given in Table I with their equation numbers in the paper and their interpretation.

4) While the proposed framework is generic and can cover a variety of related beam-centric systems such as IEEE 802.11ax/Wi-Fi 6, we give numerical results to evaluate a 5G NR-compliant radio access network (RAN) operating in a dense urban macro/picocell scenario, for both sub-6 GHz and mmWave frequencies. The results reveal the inter-dependencies between system parameters and provide insights into the associated tradeoffs.

C. Related Work

Stochastic geometry has been widely used to model and analyze several aspects of wireless networks including cellular networks [5]–[8]. A stochastic geometry framework is also popular to model mmWave cellular networks and evaluate key performance aspects such as initial access, success probability, average rate of the typical user, and the effect of blockages [9]–[12].

The study of handovers due to user mobility in non-beam-centric cellular networks and their effect on various performance metrics such as throughput is a rich area of research [13]–[15]. Most of the works have focused on BS handovers (or, equivalently, cell handovers) [16]–[23]. The work in [24] is probably the closest one to our work. This work...
TABLE II: Notation

| Symbol | Definition | Symbol | Definition |
|--------|------------|--------|------------|
| $\lambda$ | BS intensity | $c$ | MT speed |
| $f_c$ | Carrier frequency | $\phi_n$ | Speed of light |
| $q_n$ | Number of BS beams | $2^k$ | Number of MT beams |
| $\phi_{n,m}, G_{n,m}$ | Main and side lobe gains at the BS | $\phi_{b,n}$ | Beamwidth at the MT |
| $G_{n,m}$ | Main and side lobe gains at the BS | $G_{n,b}$ | Beamwidth at the MT |
| $\beta$ | SS burst periodicity | $R_c$ | LOS ball radius |
| $\alpha_1$ | LOS path-loss exponent | $\alpha_N$ | NLOS path-loss exponent |
| $W$ | Bandwidth | $\beta_0$ | Noise power density |
| $P$ | Transmit power | $\sigma^2$ | Noise power |
| $\beta$ | SIRN threshold | $Q_{\max}$ | Maximum SINR |
| $R_e$ | Ergodic Shannon rate | $\eta$ | Effective ASE |
| $T_c$ | Cell handover overhead | $T_s$ | Beam reselection overhead |
| $\mu_{c}$ | Linear intensity of BS handover | $\mu_{c}$ | Time intensity of BS handover |
| $\mu_{b}$ | Linear intensity of geometry-based beam reselection | $\mu_{b}$ | Time intensity of geometry-based beam reselection |
| $\mu_b$ | Effective intensity of beam reselection | $T_o$ | Average time overhead per unit time |
| $T_{st}$ | Geometrical time-of-stay | $T_{\text{eff},st}$ | Effective time-of-stay |
| $P_o$ | Probability of a beam switch | $P_s$ | Success probability of a transmission |

This work studies both initial beam selections during BS handovers and beam reselections within a cell and their associated overhead, in a beam-centric mmWave cellular network. The work in [24] obtains analytical expressions of inter-cell and inter-beam handover rates based on which the ASE is calculated subject to overheads due to these handovers. But, it considers only noise-limited scenarios and ignores interference from other BSs, while our work considers both noise and interference in the analysis. Second, our work also studies the effect of handovers on the number of beams during network planning phase, while [24] assumes a fixed number of beams. Third, unlike [24], we consider blockages and beam misalignment due to mobility. Finally, we also consider the directional reception at MTs and its effect on beam management. Overall, there is a lack of understanding on how network planning decisions (such as BS beamset and inter-site distance), beam management procedures (with its associated overhead) and MT mobility affect system-level performance in the presence of interference, fading, blockages, and beam misalignment error. The present paper can be seen as an attempt to incorporate all of the above in a system-level model.

II. SYSTEM MODEL

Table II provides the notation used in the paper.

A. Network Model

As shown in Fig. 1, we consider a downlink cellular network, where BS locations are modeled as a homogeneous Poisson point process (PPP) $\Phi \subset \mathbb{R}^2$ with intensity $\lambda$. We assume that a directional MT moves on a randomly oriented straight line with speed $v$. Without loss of generality, thanks to the isotropy and the stationarity of the PPP [5], this line of MT motion can be considered to be along the $x$-axis and passing through the origin. We assume that each BS always has an MT to serve. Also, a BS serves one MT at a time per resource block.\(^1\) The MT associates itself with the nearest BS. Such an association results in BS cells forming a Poisson-Voronoi tessellation as shown in Fig. 1. Let $X_0 \in \Phi$ denote the location of the serving BS of the MT at a given time. Without loss of generality, we can focus on the MT that is located at the origin at that time. After averaging over the PPP, this MT becomes the typical MT.

B. Beamforming Model

A BS at location $X \in \Phi$ uses directional beamforming to communicate with the typical directional MT located at the origin. As shown in Fig. 1, we approximate the actual antenna pattern by a sectorized one, where each sector corresponds to the main lobe of one beam of the BS. For simplicity

\(^1\) The analysis in this paper can be extended to the case where a resource block at a BS is shared by multiple MTs.
and without loss of generality, we assume that each BS has $2^n$ beams with $n \in \mathbb{N}$. This corresponds to $2^{n-1}$ beam boundaries. Hence, the beamwidth for a BS is

$$\varphi_n = \frac{2\pi}{2^n} = \frac{\pi}{2^{n-1}}.$$  (1)

We focus on a simple antenna pattern model where the main lobe is restricted to the beamwidth. Both the main and side lobe gains depend on the number $2^n$ of beams. In particular, the antenna gain $G_n$ is expressed as

$$G_n(\psi) = \begin{cases} G_{m,n}, & \text{if } |\psi| \leq \varphi_n/2 \\ G_{s,n}, & \text{otherwise,} \end{cases}$$  (2)

where $G_{m,n}$ and $G_{s,n}$ denote the antenna gains within the main lobe and the side lobe, respectively, and $\psi$ is the angle off the boresight direction. Note that the model used for beam gains in (2) is based on grid-of-beams (GoB), i.e., beam switching mode.

The beamforming model at the MT is the same as the one at the BS, where the number of beams at the typical MT is $2^k$ with $k \in \mathbb{N}$. Thus the antenna gain $G_k$ at the typical MT is expressed as (2) with the subscript ‘$n’ replaced by ‘$k’ with $\varphi_k = \frac{\pi}{2^{k-1}}$ the beamwidth at the typical MT.

C. Beam (Re)Selection

As shown in Fig. 1, the MT may cross several cell and beam boundaries as it moves on a straight line. At a cell boundary, a BS handover occurs. Thus, a new beam at the next serving BS and potentially at the MT needs to be selected during a BS handover.

Within the cell as well, the MT moves from the main lobe of one beam to that of another beam. Thus, a new beam has to be reselected at the BS and potentially at the MT as well in order for the MT to stay connected with the best serving BS beam.

Ideally, the geometry-based beam reselection would take place, where in order for the MT to stay connected with the main lobe of the best beam (as defined in Footnote 4), it should reselect the beam at a beam boundary. Such a location of beam reselection is marked by “a circle” in Fig. 2. However, due to the mobility of the MT, if the duration between two consecutive SSB bursts is sufficiently long, it is possible that the MT has moved out of the main lobe of the reference beam without selecting the new beam at the beam boundary, where the MT at time $t'$ is still connected to the side lobe of the previously selected beam at time $t$, which results in a beam misalignment.

D. Mobility-induced Beam Misalignment

Beam misalignment occurs when the main lobes of the serving BS and the typical MT are not aligned with each other. Specifically, during an SSB burst, at the serving BS, the beam that has the MT within its main lobe (i.e., the best beam) is selected for communication. We call this beam the reference beam (see Fig. 2). Due to the mobility of the MT, if the duration between two consecutive SSB bursts is sufficiently long, it is possible that the MT has moved out of the main lobe of the reference beam without selecting the new beam at the beam boundary (i.e., without performing geometry-based beam reselection).

Such a mobility-induced beam misalignment at the BS reduces the signal strength at the MT as it then lies within the side lobe of the reference beam selected during the previous SSB burst. Similar to the beam misalignment at the BS, there can be beam misalignment at the typical MT. During an SSB burst, the beam that is pointing towards the serving BS is selected at the MT to receive from the serving BS. Due to the mobility of the MT between two consecutive SSB bursts, it is possible that the beam selected at the MT during the previous SSB burst is no more pointing its main lobe towards the serving BS. As a result, the MT receives from the serving BS in the side lobe of the beam that was selected earlier in the previous

---

Footnotes:

2 The assumption of the number of beams to be $2^n$, i.e., the power of 2, is to explore a very wide range for the number of beams, from few to many (Massive-MIMO). The analysis in this paper is, however, valid for any number of beams, and not just for a number that is a power of 2.

3 Here, a beam boundary is a line segment that connects two points on the cell boundary and passes through the location of the BS, as shown in Fig. 1.

4 The best beam is the beam of the serving BS that has the MT in its main lobe. For example, as shown in Fig. 2, at time $t$, the beam represented by the solid blue line is the best beam, while at time $t'$, the beam represented by the dashed pink line is the best beam. Hence, the best beam selection is purely geometry-based and ignores reflections of signals from the BS in order to maintain the focus of the paper on the most fundamental aspects of beam management.

5 The duration between two consecutive SSB bursts is a system design parameter. If this duration is very small, we get the geometry-based beam reselection.
SSB burst. In the worst-case of beam misalignment, the side lobe of the selected beam at the serving BS is aligned with the side lobe of the selected beam at the typical MT.

At a given time, the beam misalignment probability $P_{\text{bm}}^{\text{BS}}$ at the BS depends on the speed $v$ of the MT, the duration $\tau$ between two SSB bursts, and the average distance between two consecutive BS’s beam boundaries. Here, we propose a simple approximate and yet effective formula that captures the effects of these parameters on the probability of beam misalignment at the BS due to MT mobility in a snapshot of the network. We evaluate the probability $P_{\text{bm}}^{\text{BS}}$ that the MT is outside the main lobe of the reference beam by:

$$P_{\text{bm}}^{\text{BS}} = 1 - \exp\left(-\frac{v\tau}{1/\mu_{s,b}}\right),$$

where $1/\mu_{s,b} = \frac{\pi}{2v}\sqrt{L}$ is the average distance between two consecutive BS’s beam boundaries, with $\mu_{s,b}$ being the linear intensity of beam boundary crossing given in Theorem 2 in Section IV-B. We can interpret (3) as

$$1 - P_{\text{bm}}^{\text{BS}} = \mathbb{P}(T > \tau),$$

where $T$ is an exponential random variable with mean $\frac{1}{\mu_{s,b}}$, with $T$ interpreted as the time between two consecutive SSB bursts. Note that $\frac{1}{\mu_{s,b}}$ is the average time needed by the typical MT to travel between two consecutive BS’s beam boundaries. Hence, the average time between two SSB bursts is equal to the average time taken by the typical MT to travel between two consecutive BS’s beam boundaries.

As in the case of beam misalignment on BS’s side, we use a similar formula to calculate the probability $P_{\text{bm}}^{\text{MT}}$ of beam misalignment on MT’s side as

$$P_{\text{bm}}^{\text{MT}} = 1 - \exp\left(-\frac{v\tau}{1/\mu_{s,m}}\right) = 1 - \exp\left(-\frac{\sqrt{X}}{2\tau}\right),$$

where $1/\mu_{s,m} = \frac{\pi}{2v}\sqrt{L}$ is the average distance between two consecutive MT’s beam boundaries.

Based on the beam misalignment at both the serving BS and the typical MT, the antenna gain $G_0$ of the serving BS is given by

$$G_0(n, k) = \begin{cases} 
G_{m,n}G_{m,k} \quad \text{w.p. } (1 - P_{\text{bm}}^{\text{BS}})(1 - P_{\text{bm}}^{\text{MT}}) \\
G_{m,n}G_{s,k} \quad \text{w.p. } (1 - P_{\text{bm}}^{\text{BS}})P_{\text{bm}}^{\text{MT}} \\
G_{s,n}G_{m,k} \quad \text{w.p. } P_{\text{bm}}^{\text{BS}}(1 - P_{\text{bm}}^{\text{MT}}) \\
G_{s,n}G_{s,k} \quad \text{w.p. } P_{\text{bm}}^{\text{BS}}P_{\text{bm}}^{\text{MT}}.
\end{cases}$$

E. Blockage and Channel Models

The presence of blockages leads to LOS and NLOS propagation between the MT and a BS. We adopt an LOS ball model [9] to capture the effect of blockages. The propagation between a BS and the typical MT separated by distance $d$ is LOS if $d < R_c$ where $R_c$ is the maximum distance for LOS propagation. The LOS and NLOS channel conditions induced by the blockage effect are characterized by different path-loss exponents, denoted by $\alpha_L$ and $\alpha_N$, respectively. As shown in [26], typical values of these path-loss exponents are $\alpha_L \in [1.8, 2.5]$ and $\alpha_N \in [2.5, 4.7]$.

The channel follows Rayleigh fading with unit mean power gain.\(^6\) Let $h_X$ denote the channel power gain from the BS at location $X \in \Phi$ to the MT. Note that, the random variables $h_X$ are i.i.d. exponential random variables with unit mean, i.e., $h_X \sim \exp(1)$. Let $|X|$ denote the distance between a BS at $X \in \Phi$ and the typical MT located at the origin. We consider the standard power-law path-loss model with path-loss function

$$l(X) = \begin{cases} 
K|X|^{-\alpha_L} & \text{if } |X| < R_c \\
K|X|^{-\alpha_N} & \text{if } |X| \geq R_c,
\end{cases}$$

where $K = \left(\frac{\pi}{4\pi c f_c}\right)^2$ with $c$ the speed of light and $f_c$ the carrier frequency.

F. Signal-to-interference-plus-noise Ratio (SINR)

When the typical MT is associated with the BS located at $X_0 \in \Phi$ with antenna gain $G_0$ as in (5), the SINR at the typical MT is given by

$$\text{SINR}_{n,k} = \frac{PG_0(n,k)h_{X_0}l(|X_0|)}{\sigma^2 + I_{n,k}},$$

where $P$ is the transmit power of the BS. Also, $\sigma^2 = WN_0$ is the noise power, where $W$ and $N_0$ are the bandwidth and the noise spectral density, respectively. In the denominator of (7), $I_{n,k}$ is the interference power at the typical MT given by

$$I_{n,k} = \sum_{X \in \Phi \setminus \{X_0\}} PG_X(n,k)h_{X}l(|X|),$$

where $G_X(n,k)$ is the antenna gain of an interfering BS located at $X \in \Phi$.

Since the beams of all BSs are oriented towards their respective MTs, the direction of arrivals between interfering BSs and the typical MT is distributed uniformly in $[-\pi, \pi]$. Thus, the gain $G_X$ of an interfering BS at $X \in \Phi$ is an i.i.d. discrete random variable with the probability mass function as:

$$G_X(n,k) = \begin{cases} 
G_{m,n}G_{m,k} \quad \text{w.p. } P_{\text{mm}} = \frac{\varphi_n\varphi_k}{4\pi} \\
G_{m,n}G_{s,k} \quad \text{w.p. } P_{\text{ms}} = \frac{(2\pi - \varphi_n)(2\pi - \varphi_k)}{4\pi^2} \\
G_{s,n}G_{m,k} \quad \text{w.p. } P_{\text{sm}} = \frac{(2\pi - \varphi_n)(2\pi - \varphi_k)}{4\pi^2} \\
G_{s,n}G_{s,k} \quad \text{w.p. } P_{\text{ss}} = \frac{(2\pi - \varphi_n)(2\pi - \varphi_k)}{4\pi^2},
\end{cases}$$

where $\varphi_n = \frac{\pi}{2\tau}$ and $\varphi_k = \frac{\pi}{2\tau}$ are the beamwidths of the BS and the typical MT, respectively.

III. ERGODIC SHANNON RATE

The downlink ergodic Shannon rate at the typical MT is given as

$$R(n,k) = W\mathbb{E}[\log(1 + \text{SINR}_{n,k})],$$

where $\mathbb{E}(\cdot)$ denotes expectation.

\(^6\)Although LOS mmWave channels are better modeled by Nakagami-$m$ fading, Rayleigh fading allows one much better analytical tractability. Also, simulation results in Section VIII-B (see Figs. 6 and 7) show that Rayleigh and Nakagami fading yield the same trends in terms of effective ASE.

\(^7\)The framework can also be extended to the scenario where there is a frequency reuse among BSs as described in [6].
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Lemma 1: Let

\[ F(\alpha_S, \alpha_1, w, G_0) \triangleq 2\pi\lambda \left( 1 - \frac{P_{\text{mm}}}{G_{0\text{mm}}} \right) - \frac{P_{\text{mm}}}{G_{0\text{mm}}} - \frac{P_{\text{sm}}}{G_{0\text{sm}}} - \frac{P_{\text{bs}}}{G_{0\text{bs}}} \right) w. \]  

The success probability \( p_s(n, k, \beta) \) is

\[
p_s(n, k, \beta) = \left( 1 - P_{\text{bs}} \right) \left( 1 - P_{\text{mt}} \right) q_s(n, \beta, G_{0\text{mm}}G_{0\text{sm}}G_{0\text{bs}}) + \left( 1 - P_{\text{bs}} \right) P_{\text{mt}} q_s(n, \beta, G_{0\text{mm}}G_{0\text{sm}}G_{0\text{bs}}) + P_{\text{bs}} P_{\text{mt}} q_s(n, \beta, G_{0\text{mm}}G_{0\text{sm}}G_{0\text{bs}}),
\]

where

\[
q_s(n, \beta, G_0) = \int_0^{R_c} f_R(r) \exp \left( -\frac{\beta r^\alpha \sigma^2}{P K G_0} \right) \exp \left( -\int_0^{R_c} F(\alpha_L, \alpha_L, w, G_0) \, dw - \int_\infty^{\infty} F(\alpha_N, \alpha_N, w, G_0) \, dw \right) \, dr + \int_0^{\infty} \exp \left( -\frac{\beta r^\alpha \sigma^2}{P K G_0} \right) \exp \left( -\int_0^{\infty} F(\alpha_N, \alpha_N, w, G_0) \, dw \right) f_R(r) \, dr
\]

with \( f_R(r) = 2\pi \lambda e^{-\lambda r^2} \) where \( R \) is the distance to the nearest BS, and SNR stands for signal-to-noise ratio.

Proof: The proof is given in Appendix A.

Definition 1 (Success Probability): The success probability \( p_s \) of the typical MT is the probability that the SINR at the typical MT exceeds a predefined threshold. Mathematically,

\[
p_s(n, k, \beta) \triangleq P(\text{SINR}_{n,k} > \beta),
\]

where \( \beta > 0 \) is the predefined SINR threshold, which also parametrizes the transmission rate.

We now give an analytical expression for the success probability in Lemma 1.

For sub-6 GHz bands, the expression of the success probability gets simplified, which is given in Lemma 2.

Lemma 2: For sub-6 GHz bands, the success probability \( p_s \) is given by (11) with

\[
q_s(n, \beta, G_0) = \int_0^{\infty} f_R(r) \exp \left( -\frac{\beta r^\alpha \sigma^2}{P K G_0} \right) \exp \left( -\int_0^{\infty} F(\alpha_N, \alpha_N, w, G_0) \, dw \right) \, dr.
\]

Proof: The desired expression of the success probability is obtained by substituting \( R_c = \infty \) and replacing \( \alpha_L \) with \( \alpha_N \) in (12).

Theorem 1: Imposing the limit \( Q_{\text{max}} \) on the maximum achievable SINR stemming from RF imperfections and modulation schemes, the ergodic Shannon rate per unit time is

\[
\mathcal{R}(n, k) = W \int_0^{Q_{\text{max}}} \frac{p_s(n, k, z)}{z+1} \, dz,
\]

where \( p_s(n, k, z) \) is given by (11).

Proof: The proof follows directly from

\[
\mathcal{R}(n, k) = W \int_0^{\infty} P(\log(1 + \min(\text{SINR}_{n,k}, Q_{\text{max}})) > z) \, dz = W \int_0^{Q_{\text{max}}} p_s(n, k, e^z - 1) \, dz = W \int_0^{Q_{\text{max}}} \frac{p_s(n, k, z)}{z+1} \, dz.
\]

IV. Beam (Re)Selection

A. Beam Selection during BS Handovers

When the MT performs a BS handover, a beam is selected with the new BS as well as the typical MT. We know from [28] that, for the Poisson-Voronoi tessellation, the linear intensity of cell boundary crossing, i.e., BS handovers, is \( \mu_{\text{bc}} = \frac{4\sqrt{\lambda}}{\pi} \).

Theorem 2: Imposing the limit \( Q_{\text{max}} \) on the maximum achievable SINR stemming from RF imperfections and modulation schemes, the ergodic Shannon rate per unit time is

\[
\mathcal{R}(n, k) = W \int_0^{Q_{\text{max}}} \frac{p_s(n, k, z)}{z+1} \, dz,
\]

where \( p_s(n, k, z) \) is given by (11).

Proof: The proof follows directly from

\[
\mathcal{R}(n, k) = W \int_0^{\infty} P(\log(1 + \min(\text{SINR}_{n,k}, Q_{\text{max}})) > z) \, dz = W \int_0^{Q_{\text{max}}} p_s(n, k, e^z - 1) \, dz = W \int_0^{Q_{\text{max}}} \frac{p_s(n, k, z)}{z+1} \, dz.
\]

Theorem 3: Imposing the limit \( Q_{\text{max}} \) on the maximum achievable SINR stemming from RF imperfections and modulation schemes, the ergodic Shannon rate per unit time is

\[
\mathcal{R}(n, k) = W \int_0^{Q_{\text{max}}} \frac{p_s(n, k, z)}{z+1} \, dz,
\]

where \( p_s(n, k, z) \) is given by (11).

Proof: The proof follows directly from

\[
\mathcal{R}(n, k) = W \int_0^{\infty} P(\log(1 + \min(\text{SINR}_{n,k}, Q_{\text{max}})) > z) \, dz = W \int_0^{Q_{\text{max}}} p_s(n, k, e^z - 1) \, dz = W \int_0^{Q_{\text{max}}} \frac{p_s(n, k, z)}{z+1} \, dz.
\]

Theorem 4: Imposing the limit \( Q_{\text{max}} \) on the maximum achievable SINR stemming from RF imperfections and modulation schemes, the ergodic Shannon rate per unit time is

\[
\mathcal{R}(n, k) = W \int_0^{Q_{\text{max}}} \frac{p_s(n, k, z)}{z+1} \, dz,
\]

where \( p_s(n, k, z) \) is given by (11).

Proof: The proof follows directly from

\[
\mathcal{R}(n, k) = W \int_0^{\infty} P(\log(1 + \min(\text{SINR}_{n,k}, Q_{\text{max}})) > z) \, dz = W \int_0^{Q_{\text{max}}} p_s(n, k, e^z - 1) \, dz = W \int_0^{Q_{\text{max}}} \frac{p_s(n, k, z)}{z+1} \, dz.
\]
Hence, the time intensity of BS handover (or, equivalently, beam selection) is
\[
\mu_c = \frac{4\sqrt{\lambda}}{\pi}v. \tag{16}
\]

B. Beam Reselection Within the Cell

We now calculate the average number of beam reselections the typical MT performs per unit length and the time intensity of beam reselection, i.e., the average rate of beam reselections. As discussed in Section II-C, the beam reselection events are a combination of geometry- and measurement-based beam reselection events.

Recall that a geometry-based beam reselection occurs at a beam boundary within the Voronoi cell of a BS. In Fig. 1, locations of geometry-based beam reselections are denoted by the “circles on dashed lines.”

**Theorem 2 (Intensity of geometry-based beam reselection):** For \(2^n\) beams at a BS and PPP of intensity \(\lambda\), the linear intensity \(\mu_{a,b}\) of geometry-based beam reselection for the typical MT moving on a straight line with speed \(v\) is \(\frac{2^n\sqrt{\lambda}}{\pi}\), while the time intensity \(\mu_{t,b}\) is
\[
\mu_{t,b}(n) = \frac{2^n\sqrt{\lambda}}{\pi}v. \tag{17}
\]

**Proof:** The proof is given in Appendix B. \(\blacksquare\)

This theorem is valid when integrating over all motion directions of the MT chosen uniformly at random, and it does not hold for a fixed direction of MT motion.

**Corollary 1:** When taken into account the average number of geometry-based beam reselections that are skipped between two consecutive SSB bursts, the effective time intensity of beam reselection becomes
\[
\mu_{b}(n) = \frac{1}{\max(\tau, \frac{1}{\mu_{t,b}(n)})}, \tag{18}
\]
where \(\tau\) is the SSB burst periodicity.

**Corollary 2:** The geometry-based time-of-stay \(T_{st}\) of the MT defined as the average time spent by the MT within the main lobe of a beam is simply the inverse of the time intensity \(\mu_{t,b}\), i.e.,
\[
T_{st} = \frac{1}{\mu_{b}} = \frac{\pi}{2^n\sqrt{\lambda}v}. \tag{19}
\]

**Corollary 3:** The effective time-of-stay \(T_{eff,st}\) defined as the average time for which the MT is connected with a beam of the BS is
\[
T_{eff,st} = \frac{1}{\mu_{b}(n)} = \max\left(\tau, \frac{1}{\mu_{t,b}(n)}\right). \tag{20}
\]

C. Time Overheads due to Beam (Re)Selection

This subsection builds on the previous subsections on analytical results for beam (re)selections and incorporates the practical time overheads that arise from the 5G NR design.

BS handovers and beam reselections may result in significant overheads in terms of additional delay required for periodically conducting the SSB measurement and report which are required for the SSB beam sweeping and beam alignment procedures. Such an overhead in time reduces the overall time available for data transmissions, in turn reducing the ergodic Shannon rate.

The two components that contribute to the time overhead are:

1) The time \(T_c\) for executing the simultaneous cell and beam reselection procedures during each BS handover at cell boundary crossing. This includes the periodic SSB measurement, receiver processing time for the SSBs, and the handover interruption time due to cell switch and radio resource control (RRC) reconfiguration.

2) The time \(T_{b}\) for beam alignment after each beam reselection within the cell of a BS, which includes the periodic SSB measurement and the receiver processing time for the SSBs.

Below we describe a step-by-step procedure for beam selection during a BS handover:

1) A BS transmits a sequence of SSB bursts periodically, where each SSB in an SSB burst uses a different BS beam.

2) The MT measures the SSBs in the SSB bursts transmitted periodically by the BS and track which of the SSBs in the SSB burst presents the highest Reference Signal Received Power (RSRP) for the BS, i.e., which of the BS beams presented the best RSRP during the SSB burst.

3) The MT then assumes that the best serving BS beam is the BS beam that presented the best RSRP during the last SSB burst.

4) The cell mobility is based on measurements on the best serving BS beam for the serving cell and the neighbor target BSs.

5) The beam reselection is based on measurements for the best serving BS beam on the serving BS.

Now, we give time overheads corresponding to each operation in the beam selection protocol during a BS handover:

1) We assume the SSB burst periodicity to be 20 ms; this is one of the values specified by the 3GPP standard [3], [4].

2) The assumed RRC processing delay is 3 ms.

3) The assumed handover processing delay for the Random Access Channel (RACH) procedure is 20 ms.

Thus we assume that the BS handover time overhead \(T_c\) is 43 ms.

Corresponding to the intra-cell mobility of the MT, we now describe each operation for a beam reselection with corresponding time overheads.

1) The beam reselection overhead is the SSB burst period (20 ms)

2) The RRC processing delay (3 ms)

This leads to 23 ms of time overhead \(T_b\) per beam reselection.

There is also a scaling factor for those SSB measurement delays, associated with the way the MT implements the SSB measurements, which is intrinsically related to its number of antenna panels and their associated baseband processing chains. In particular, the 3GPP specifies several multi-panel...
Fig. 3: Probabilistic beam switching with two beams (panels) at the MT. The triangles depict the BSs located according to a PPP. The solid black lines denote cell boundaries. A “cross” denotes the BS handover location of the MT. P1, P2, and P3 denote randomly oriented panels of the MT pertaining to each BS handover location, where each of the two beams covers the left and right halves separated by the panel. For instance, the BSs X₁ and X₂ lie in the coverage of two different beams, i.e., on the opposite side of the panel P₁. Thus there will be a beam switch during the handover from X₁ to X₂. On the contrary, X₂ and X₃ lie in the coverage of the same beam (the left beam). Thus there is no need of a beam switch during the handover from X₂ to X₃.

2) Full Overhead Case: This case corresponds to MPUE-Assumption #1, where there is a single baseband processing unit that needs to be shared by all of the \(2^k\) beams at the typical MT. Thus the SSB measurement for each of the \(2^k\) beams is done sequentially. In this case, the total average overhead per unit time is

\[
T_o(n) = 2^k (\mu_b(n)T_b + \mu_cT_c).
\]

Here, the average overhead per unit time is \(2^k\) times the one in the limited overhead case, but with an advantage of significantly less hardware complexity at the MT.

A key disadvantage of the full overhead case is that the beam measurement is done during a BS handover even if the current serving BS and the next serving BS lie in the coverage of the same MT beam. Thus we propose a probabilistic beam switch case that uses the network geometry, namely, BS locations to reduce the overhead compared to the full overhead case.

3) Probabilistic Beam Switch: The idea is to predict the possibility of a beam switch during a BS handover since a beam switch is necessary if and only if the current and the next serving BSs lie in the coverage of different MT beams. The case of two beams at the MT is depicted in Fig. 3. Exploiting the properties of the PPP that models BS locations, the probability that the current and the next serving BSs lie in different beams can be calculated [29]. Specifically, when there are \(2^k\) beams at the typical MT with main lobes oriented in uniformly at random directions and covering all directions, the probability of a beam switch is [29, Corollary 3]

\[
p_{sw} = \frac{\pi}{2^k} \sin \frac{2^k}{\pi}, \quad k \geq 1.
\]

Alternatively, only \(p_{sw}\) fraction of BS handovers require a beam switch. When there are two, four, or eight beams at the MT, the probability of a beam switch during a BS handover is 0.637, 0.9, and 0.975, respectively. As a result, the total average overhead per unit time can be given by

\[
T_o(n) = 2^k \mu_b(n)T_b + (p_{sw}2^k + 1 - p_{sw})\mu_cT_c.
\]
TABLE III: Network parameter values for FR1 and FR2 deployments [3], [4]

| Parameter                        | FR1                            | FR2                            |
|----------------------------------|---------------------------------|---------------------------------|
|Carrier frequency ($f_c$)         | 3.5 GHz                         | 28 GHz                         |
|Bandwidth (W)                     | 100 MHz per carrier             | 400 MHz per carrier             |
|Noise density ($N_0$)             | $-174$ dBm/Hz                   | $-174$ dBm/Hz                   |
|Transmit power ($P$)              | 43 dBm                         | 36 dBm                         |
|Beam reselection overhead ($T_{b}$)| 23 ms                           | 23 ms                           |
|Cell handover overhead ($T_{c}$)  | 43 ms                           | 43 ms                           |
|SSB burst periodicity ($)         | 20 ms                           | 20 ms                           |
|MT speed ($v$)                    | [4, 30, 120] km/h               | [4, 30, 120] km/h               |
|Inter-site distance (ISD)         | [250, 500, 1000] m              | [75, 125, 250] m                |
|Maximum SINR ($Q_{\text{max}}$)   | 30 dB                           | 30 dB                           |
|Path loss exponent ($\alpha$)     | 3.5                             | $\alpha_L = 1.9, \alpha_N = 3.5$|
|Blockage model                    | Implicit (NLOS)                 | LOS ball                        |
|LOS ball radius ($R_b$)           | –                               | 75 m                            |

V. EFFECTIVE AREA SPECTRAL EFFICIENCY

For each of the three overhead cases discussed in Section IV-C, the effective ASE per unit time is

$$R_{\text{eff}}(n, k) = \lambda(1 - T_o(n))^{+} R(n, k),$$

where $R(n, k)$ is given by (14) and $(A)^+ = \max(0, A)$.

For a given $k$, our objective is to find the integer $n$ that maximizes the effective ASE per unit time, i.e.,

$$n_\ast = \arg\max_{n \in \mathbb{N}} R_{\text{eff}}(n, k).$$

The value of $n_\ast$ can easily be found by a linear search.

VI. NETWORK SETUP

To validate our proposed model, we consider a 5G NR-compliant radio access network (RAN) operating in a dense urban macro/pico cell scenario. A summary of the model parameters for FR1 (sub-6 GHz) and FR2 (above 6 GHz) network deployments is provided in Table III.

To explore the best potential of 5G NR networks in operational bands FR1 and FR2, we use the maximum bandwidth allowed as per 5G NR Release 15 [3], [4], namely 100 MHz per carrier for FR1 and 400 MHz per carrier for FR2. For FR1, we assume NLOS conditions.

As the inter-site (or, equivalently inter-BS) distances (ISDs) for FR1 are expected to be larger due to lower frequency-dependent path loss, we choose a transmission power $P = 43$ dBm. For FR2, we can expect smaller ISDs due to (a) higher attenuation loss at higher carrier frequencies, and (b) because massive MIMO and high beamforming gains imposes challenges in terms of RF exposure and EMF limitations. Thus we decrease $P$ to 36 dBm.

An important parameter is the intensity $\lambda$ of BSs, which is related to the average cell size and the ISD. For an intensity $\lambda$ of BSs, the average cell size is $1/\lambda$. The average cell radius is defined as the radius $r_{\text{cell}}$ of a ball having the same average area as the cell: $1/\lambda$. Then, the average ISD is $2r_{\text{cell}} = 2/(\pi \lambda)$. Hence we simply adjust the value of the intensity $\lambda$ of BSs to represent different ISD scenarios. For FR1 bands, we analyze the following ISDs: 1000 m, 500 m, and 250 m. As for FR2 bands, the effect of propagation attenuation requires us to decrease the ISD. Hence we consider the following ISDs: 250 m, 125 m, and 75 m.

One important network planning decision is the number of beams per BS and per MT. In our model, this is related to the choice of the values for $n$ and $k$, respectively. The main and side lobe gains depend on the number $2^n$ and $2^k$ of beams. Specifically, an increase in the number of beams increases the main lobe gain and decreases the side lobe gain. Thus, without loss of generality, we assume the following antenna gains. The main lobe gain is $G_{m,n} = 2^n$ at a BS ($G_{m,k} = 2^k$ at the MT), while the side lobe gain is $G_{s,n} = 1/2^n$ at a BS ($G_{s,k} = 1/2^k$ at the MT).

VII. NUMERICAL RESULTS: OMIDIRECTIONAL MT

We now demonstrate how the proposed model can be used for system-level evaluation of the effect of different system parameters on 5G NR network deployments over FR1 and FR2 for the omnidirectional MT for different MT speeds $v$ and ISDs (in Figs. 4a, 4b, and 5). In Section VIII, we will consider the case of the directional MT that has $2^k$, $k \geq 1$ beams. The discussions in this section pertain to Figs. 4a, 4b, and 5.

A. Effect of the Number of Beams at BSs

In both FR1 and FR2 deployments, for a given ISD, as $n$ (and hence the number $2^n$ of beams) increases, the beam-forming gain increases and the interference from interfering BSs decreases due to narrower beams. But, at the same time, for a given $v$, the typical MT performs more frequent beam reselections due to a smaller beamwidth, increasing the time overhead. The negative impact of the increased time overhead gradually dominates the beamforming gain. Also, an increase in $n$ increases the probability of beam misalignment at the BS (given by (3)) as the MT is more likely to move into the beamwidth of another beam between two consecutive SSB measurements. As a result of this tussle between the increased beamforming gain, increased time overhead due to beam reselections, and the increased probability of beam misalignment, we observe that there is a value $n_\ast$ of $n$ that maximizes the effective ASE.

10As seen from previous sections, our model is amenable to different modeling of antenna gain patterns.
B. Effect of the MT Speed

With an increase in \( v \), the MT crosses beam and cell boundaries more frequently resulting in a higher number of beam reselections and BS handovers, respectively. Also, the probability of beam misalignment increases. Hence, with an increase in \( v \), the optimal value \( n^* \) decreases, and for a fixed \( n \), the effective ASE decreases.

C. Effect of the ISD

Note that a smaller ISD means a denser cellular network. As the ISD increases, the average cell size increases. Thus, BSs need to increase the number \( 2^n \) of beams for a higher beamforming gain (equivalently, a smaller beamwidth) and smaller interference. Hence, the value of \( n^* \) increases with ISD. For a smaller \( n \), the time overhead associated with beam reselections is small. Hence, a smaller ISD results in a higher effective ASE due to a smaller distance between the typical MT and its serving BS. This dominates the negative effects of increased interference power due to a denser deployment of BSs and increased time overhead due to more frequent BS handovers. But, for a large \( n \), both beam reselections and BS handovers happen more frequently for a smaller ISD, and the network with a larger ISD achieves a higher effective ASE.

D. Comparison of FR1 and FR2 Deployments

When comparing beamwidths for FR1 with those for FR2 given the same \( n \) value, we can expect that, even though the angular beamwidth for a given \( n \) is the same, the linear width of beams will be larger in FR1 than that in FR2 due to a usually larger cell radius in the former.\(^{11}\) Thus, it is expected that MTs operating in FR1 are less penalized due to overheads associated with beam reselections and BS handovers. Also, due to a larger ISD, the distance-based path loss when operating in FR1 is higher than when operating in FR2. Hence for the same value of \( n \), we can expect that the interference in FR1 is smaller than that in FR2 despite a bit higher transmit power in FR1. This indicates that the additional received interference from a higher number of beams is not as intense in FR2 as in FR1. As shown in Fig. 5, this behavior is captured by our model, where the optimal value \( n^*_s \) for the ISD = 250 m in FR1 (\( n^*_s = 8 \)) is higher than that in FR2 (\( n^*_s = 6 \)) with ISD = 75 m or in FR2 with ISD = 125 m (\( n^*_s = 7 \)).

Also, as Fig. 5 shows, when we compare the performances of FR1 and FR2 deployments for the same ISD, we observe an interesting tradeoff. Smaller ISDs (e.g., 75 m) benefit FR2 irrespective of the value of \( n \) as, for a given critical LOS distance \( R_c \), it is more likely that the serving BS has

\(^{11}\)Although nothing prohibits small ISDs for FR1 (e.g., Wi-Fi operation in 2.4 GHz and 5 GHz), pico/femto cell deployment models are the best fit for mmWave deployments.
LOS propagation to the MT (so smaller path loss) boosting signal power. Recall that, in FR1, even the serving BS always has NLOS propagation to the MT. As a result, the impact of increased time overheads with $n$ on the effective ASE is less in FR2 than that in FR1. As the ISD increases, the probability of serving BS lying outside the LOS ball increases, in turn, reducing signal power significantly in FR2. Thus, when combined with higher path loss at higher frequencies in FR2, for higher values of $n$, the impact of time overheads is relatively higher in FR2 than FR1. Note that, as a result of the tussle between competing effects, the values of $n_*$ in FR1 and FR2 are close to each other for the same ISD.

Overall, the numerical results discussed in this section validate the claim that the proposed model allows for a system-level evaluation of network planning decisions in beam-based access networks such as 5G NR.

Note that, although the discussions on the effect of number of beams at the BS, MT speed, and the ISD on the effective ASE have considered until now an omnidirectional MT, they are also valid for the case of directional MT.

VIII. NUMERICAL RESULTS: DIRECTIONAL MT

We now study the effect of multiple beams at the typical MT and associated systemic tradeoffs. We will also compare the performance of the directional MT with that of the omnidirectional MT. Since it is expected that multiple beams at the MT will be used mostly in FR2 (mmWave) due to the need of directional communications, we restrict our discussion to FR2.

A. Effect of the Number of Beams at the MT

Figs. 6 and 7 depict, for different ISDs and fading models, the systemic tradeoffs associated with the directional MT and the effect of the number of baseband processing chains discussed in Section IV-C. Recall that, as given by (21), (22), and (24), the time overheads for the limited overhead (LO) case and the omnidirectional MT are the same, and are smaller when compared to the probabilistic overhead (PO) and full overhead (FO) cases, with the FO case leading to the highest time overhead. Specifically, Figs. 6 and 7 compare the performance of the directional MT with two ($k = 1$) and four ($k = 2$) directional beams with the omnidirectional MT. For the LO case, the additional beamforming gain due to multiple directional beams at the MT (in addition to the beamforming gain at the BS) dominates consistently over the omnidirectional MT case, as the time overhead due to multiple beams at the MT remains constant for the LO case irrespective of the number $2^k$ of beams at the MT. In other words, for all values of $n$, the LO case with four beams at the MT performs best, and the LO case with two beams outperforms the omnidirectional MT case. Although the probability of beam misalignment at the MT increases with $k$ (see (4)), the beamforming gain dominates this performance deteriorating factor.

On the other hand, for the FO case, the time overhead increases proportionally to both the number $2^k$ of beams at the MT as well as the number $2^n$ of beams at the BS (see (22)). Thus, after a certain value of $n$, the beamforming gain at the MT is eventually dominated by the increased time overhead and the probability of beam misalignment at both the MT and the BS. For instance, as shown in Fig. 6a, for $2^5 = 32$ beams at the BS, the case with four beams at the MT achieves better effective ASE compared to the case with two beams at the MT, and the trend reverses from $2^6 = 64$ beams onwards at the BS. Also, for the FO case, when the number $2^n$ of beams at the BS is large enough (e.g., 32 beams in Fig. 6a), the advantage of the directional communication at the MT vanishes due to the increased time overhead, and the omnidirectional reception at the MT leads to the better effective ASE. The optimal value of $n$ that maximizes the effective ASE reduces with an increase in $k$ in order to balance between the positive effect of the...
beamforming and the negative impact of the increased time overhead and the increased probability of beam misalignment. For a given number of beams at the MT, i.e., for fixed $k$, the PO case offers an advantage over the FO case due to a smaller number of beam switching at the MT for the given set of network parameters.

To determine the effect of fading on the performance, we compare two fading models: Rayleigh and Nakagami-$m$. For the latter, we assume that the LOS propagation is characterized by Nakagami-4 fading. As shown in Figs. 6 and 7, both fading models present the same performance trend in the effective ASE for different number of beams at the BS and the MT, ISDs, and the overhead cases. This confirms the interest of our mathematical results based on Rayleigh fading.

As Figs. 6 and 7 together show, the effect of the ISD for the directional MT is the same as that for the omnidirectional MT (discussed in Section VII-C). With respect to the directional MT case, the comparison of Figs. 6 and 7 reveals that the crossover point, where the FO case with four beams at the MT ($k = 2$) starts performing worse compared to the FO case with two beams at the MT ($k = 1$) and to the omnidirectional MT, shifts towards right with an increase in ISD as the influence of the beamforming gain increases due to larger average cell sizes.

Fig. 8 gives a general view of the effect of directional communications from the perspectives of both the BS and the MT. Specifically, it gives the optimal number of beams at the BS as well as the MT using a 2-D numerical optimization.
B. Network Performance for the Mix of MTs

Fig. 9 compares a homogeneous network consisting of only MTs with four beams ($k = 2$) and a heterogeneous network consisting of a mix of MTs traveling at the same speed of $v = 30$ km/h. For the heterogeneous network, 60% of the MTs are omnidirectional ($p_0 = 0.6$), 30% of the MTs are with two beams ($p_1 = 0.3$), and 10% of the MTs are with four beams ($p_2 = 0.1$). The performance for the mix of the MTs can be obtained by weighing the ergodic Shannon rate given by (14) by the probabilities $p_0$, $p_1$, and $p_2$.

Specifically, for the LO case, the homogeneous network of MTs with four beams suffers from a loss in the effective ASE if other types of MTs are to be added in that network. This is an expected result as the MTs with two beams and the omnidirectional MTs achieve a smaller beamforming gain, while the time overhead due to multiple beams at the MT remains the same irrespective of the type of the MT. On the other hand, for the FO case, the design of the network is more complicated. In particular, Fig. 9 depicts how the number of beams at the BS must be adjusted depending on the composition of the network. For instance, when the network consists of only MTs with four beams, having a small number beams at the BS is beneficial from the effective ASE point of view. On the contrary, if the network is heterogeneous as per the aforementioned composition, having a large number of beams at the BS is beneficial.

Fig. 10 captures the overall performance of the network consisting of a mix of MTs where 60% of MTs move at 3 km/h ($q_3 = 0.6$), while 40% move at 30 km/h ($q_{30} = 0.4$). For each type of MT in terms of speed, 60% of the MTs are omnidirectional ($p_0 = 0.6$), 30% of the MTs have two beams ($p_1 = 0.3$), and 10% of the MTs are with four beams ($p_2 = 0.1$). In such a network, $2^n = 512$ beams are required at the BS to maximize the effective ASE for the LO case, while $2^n = 256$ beams are sufficient for the FO case. Note that, despite of large time overhead in the FO case compared to the LO case, the optimal effective ASE achieved in the former case (137.9 nats/s/Hz/km²) is close to that in the latter case (142.3 nats/s/Hz/km²). Recalling that the FO case has reduced hardware complexity compared to the LO case, Fig. 10 implies that the network operator might be able to provide almost the same quality of service to MTs at reduced hardware complexity for certain network compositions.

IX. CONCLUSIONS AND FUTURE DIRECTIONS

The system-level mathematical framework for beam management in 5G RAN presented in this paper captures

- essential scenario characteristics (e.g., operational frequency, blockage characteristics)
- technological features (e.g., beamforming configuration, delay overheads)
- network deployment choices (e.g., ISD, carrier bandwidth)
- traffic scenarios (e.g., mix of MTs).

Also, this framework leads to the definition of several new key performance metrics proper to 5G NR RANs; stochastic geometry was used to derive closed-form expressions of

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Fig. 9: Heterogeneous vs. homogeneous networks. $v = 30$ km/h and ISD = 200 m. $p_0 = 0.6$, $p_1 = 0.3$, and $p_2 = 0.1$.

Fig. 10: Overall performance for the mix of MTs. ISD = 200 m. $p_0 = 0.6$, $p_1 = 0.3$, and $p_2 = 0.1$. $q_3 = 0.6$ and $q_{30} = 0.4$.

For the LO case, the optimal number of beams at the MT is $2^9 = 512$, while it is $2^6 = 64$ at the BS. This is due to the fact that, for the LO case, the time overhead does not increase with the number of beams at the MT. Thus, it is better to increase the number of beams at the MT instead of at the BS to achieve sufficient beamforming gain. However, the negative impact of increased probability of beam misalignment eventually dominates, which reduces the effective ASE after increasing the number of beams beyond 256 at the MT.\(^{12}\) On the other hand, as Fig. 8b shows, the optimal number of beams at the MT reduces to four for the FO case as a result of the proportional increase in the time overhead with the number of beams at the MT.

\(^{12}\)As of now, having 256 beams at the MT may be infeasible, but it may be a reality in the future, especially for MTs that are not smartphones, such as flying drones and vehicles.
each of them. These expressions are then aggregated in a global formula allowing one to evaluate the effective area spectral efficiency of this 5G RAN. This effective area spectral efficiency is the Shannon rate per Hertz averaged out over all users of a large network, when taking into account both the pros of beam densification in terms of improved SINR, and its cons in terms of the handover overheads that are incurred by mobile users when they switch beams or cells. For a dense urban macro/pico cell scenario in sub-6 GHz and mmWave bands, the framework accurately captures the systemic tradeoffs between ISDs, path loss, interference, and signaling overhead due to beam management.

In the future, the model can be improved to incorporate sectorized BSs with antenna panels and their effects on beam shaping/gains, MT blockage models, and others. Further, our model can be extended to capture other tradeoffs involved in designing a beam-based RAN. For instance, the average beam time-of-stay, i.e., the time a user remains with a given beam before switching to another beam, decreases with an increase in the number of beams in the beamset, which impacts the available time for performing channel estimation, link adaptation, and power control. Also, decreasing the periodicity interval in which beamformed reference signal resources are monitored may improve the effectiveness and response time of beam refinement, but at the same time it results in reduced spectral efficiency due to the control overhead.

From a theoretical analysis perspective, our framework can be improved and extended in several ways by modeling the LOS/NLOS propagation in a more sophisticated manner as in [10], analyzing for arbitrarily shaped MT path, extending to multi-tier networks, and calculating exactly the probability of beam misalignment for the Poisson geometry of BSs. Furthermore, more realistic beam patterns could be considered to take into account non-uniform beamwidths, arbitrary beamwidth distributions, and a connection between the BS and the MT through an NLOS beam due to reflections. Finally, our framework is supposed to complement system-level simulations; an actual validation of the framework using system-level simulations is left for future research.

**APPENDIX A**

**PROOF OF LEMMA 1**

Based on whether the serving BS lies within the LOS ball of radius \( R_c \) or not, we can write the success probability \( p_s \) as

\[
p_s(n, k, \beta) = \int_0^{R_c} \mathbb{P}(\text{SINR}_{n,k} > \beta \mid r) f_R(r) dr + \int_{R_c}^\infty \mathbb{P}(\text{SINR}_{n,k} > \beta \mid r) f_R(r) dr,
\]

where \( f_R(r) = 2\pi \lambda r e^{-(\lambda \pi r^2)} \) is the probability density function of the distance \( R \) of the typical MT to the nearest BS. When \( 0 < r < R_c \), we have

\[
\mathbb{P}(\text{SINR}_{n,k} > \beta \mid r) = \mathbb{P} \left( \frac{PKG_0 h_{X_t} r^{-\alpha L}}{\sigma^2 + h_{I_n}} > \beta \mid r \right) \\
= \mathbb{P} \left( h_{X_t} > \frac{\beta \alpha L}{PKG_0} (\sigma^2 + h_{I_n}) \mid r \right) \\
= e^{-\frac{\beta \alpha L}{PKG_0} I_{n,k}} \mathbb{E} \left[ \exp \left( -\frac{\beta \alpha L}{PKG_0} I_{n,k} \right) \right]
\]

for a given \( G_0 \) which is a random variable with the probability mass function given by (5).

We have

\[
E \left[ \exp \left( -\frac{\beta \alpha L}{PKG_0} I_{n,k} \right) \right] = E \left[ \exp \left( -\frac{\beta \alpha L}{PKG_0} \sum_{X \in \Phi \setminus \{X_0\}} PG X h_X l(|X|) \right) \right]
\]

\[
\quad = E \left[ \prod_{X \in \Phi \setminus \{X_0\}} \exp \left( -\frac{\beta \alpha L}{PKG_0} G X h_X l(|X|) \right) \right]
\]

\[
\quad = \mathbb{E} \left[ \prod_{X \in \Phi \setminus \{X_0\}} \left( 1 + \frac{1}{1 + \frac{\beta \alpha L}{PG_0} G X h_X l(|X|)} \right) \right]
\]

\[
\quad + \mathbb{E} \left[ \prod_{X \in \Phi \setminus \{X_0\}} \left( \frac{p_{mm}}{1 + \frac{\beta \alpha L}{PG_0} G X h_X l(|X|)} \right) \right]
\]

\[
\quad + \mathbb{E} \left[ \prod_{X \in \Phi \setminus \{X_0\}} \left( \frac{p_{mm}}{1 + \frac{\beta \alpha L}{PG_0} G X h_X l(|X|)} \right) \right],
\]

where (a) follows from the i.i.d. nature of fading random variables, (b) follows from averaging over the channel power gains on interfering channels, and (c) follows from the probability mass function of the gain \( G_X \) (given by (9)) of an interfering BS at \( X \in \Phi \).

From the probability generating functional (PGFL) of PPP, it follows that

\[
E \left[ \exp \left( -\frac{\beta \alpha L}{PKG_0} I_{n,k} \right) \right] = \exp \left( -2\pi \lambda \int_0^\infty \left( 1 - \frac{p_{mm}}{1 + \frac{\beta \alpha L}{PG_0} G_{mm} G_{m,k}} \right) dw \right)
\]

\[
\quad - \frac{p_{mm}}{1 + \frac{\beta \alpha L}{PG_0} G_{mm} G_{m,k}} w \left( \int_0^\infty F(\alpha_L, \alpha_L, w, G_0) dw \right)
\]

\[
\quad - \int_{R_c}^\infty F(\alpha_L, \alpha_N, w, G_0) dw,
\]

where, in (28), the first integral corresponds to interfering BSs within the LOS ball and the second integral to those outside the LOS ball with \( F(\alpha_S, \alpha_L, w, G_0) \) given by (10).
Similarly, one can obtain an expression for $\Pr(\text{SINR}_m > \beta \mid r)$ when $R_c \leq r < \infty$, where the interfering BSs lie outside the LOS ball. By averaging over the distance $R$ of the typical MT to its nearest BS, one gets (12). Finally, averaging over the gain $G_0$ from the serving BS yields the final expression of the success probability in (11).

**Appendix B**

**Proof of Theorem 2**

Geometry-based beam reselections occur at beam boundaries of a BS. In Fig. 1, these locations of beam reselections are denoted by “circles.” Let $\theta$ denote the angle of a beam boundary with respect to the direction of the motion of the MT (see Fig. 11). This angle $\theta$ is distributed uniformly at random in $[0, \pi]$. In Fig. 11, a “circle” denotes a point along the $x$-axis where the typical MT reselects the beam. Let $\Psi \subseteq \mathbb{R}$ denote the point process of beam reselection events, where the points of $\Psi$ are indicated by “circles.” We are interested in calculating the average number of beam reselections the typical MT performs per unit length, which is equivalent to calculating the intensity of $\Psi$.

Without loss of generality, consider the motion of the typical MT in the interval $[0, \ell]$, which corresponds to the motion of the typical MT from $(0,0)$ to $(\ell,0)$ along the $x$-axis. First, we calculate the average number of beam reselections when there is at most one beam reselection corresponding to a BS. This happens when there are two beams of the same size for a BS. Using the result for two beams, we can obtain the intensity of beam reselection corresponding to $2^n$ beams at a BS.

During the interval $[0, \ell]$, the typical MT may move through the Voronoi cells of multiple BSs. As shown in Fig. 12, let $\omega(X)$ denote the point of the beam reselection corresponding to the BS located at $X \in \Phi$. The event of beam reselection corresponding to a BS at $X \in \Phi$ occurs when the following two events occur simultaneously:

1) the point of the beam reselection lies in the Voronoi cell of the BS at $X \in \Phi$, i.e., $\omega(X) \in V_\Phi(X)$ where $V_\Phi(X)$ is the Voronoi cell of the BS located at $X \in \Phi$.

2) the point of the beam reselection lies on the line connecting $(0,0)$ and $(\ell,0)$, i.e., $\omega(X) \in [0,\ell]$.

Consequently, conditioning on $\theta$, the average of number of beam reselections in $[0, \ell]$ is

$$\mathbb{E}(\Psi[0,\ell] \mid \theta) = \lambda \int_{\mathbb{R}^2} \Pr_z(\omega(z) \in V_\Phi(z)) \mathbb{1}_{\omega(z) \in [0,\ell]} \, dz,$$

where $\Pr_z(\cdot)$ denotes the Palm probability.

**Event $\omega(z) \in V_\Phi(z)$**: This event occurs when there is no BS closer to the typical MT than the one at location $z$. This is equivalent to the event that there is no BS in the ball of radius $|z - \omega(z)|$ centered at $\omega(z)$. Since the BS point process is a PPP with intensity $\lambda$, we have

$$\Pr_z(\omega(z) \in V_\Phi(z)) = \exp(-\lambda \pi \|z - \omega(z)\|^2) = \exp\left(-\frac{\lambda \pi y^2}{\sin^2 \theta}\right),$$

(30)

where $\|z - \omega(z)\| = \frac{y}{\sin \theta}$ since $z = (x,y)$. 

**Event $\omega(z) \in [0,\ell]$**: This event occurs if the BS at $z$ lies within the strip $\mathcal{S}$ between two lines passing through the origin $(0,0)$ and $(\ell,0)$ at angle $\theta$ as shown in Fig. 12. Equivalently, by representing $z$ in Euclidean coordinates as $z = (x,y)$, it follows that

$$\mathbb{1}_{\omega(z) \in [0,\ell]} \, dz = 1_{z \in \mathcal{S}} \, dz = 1_{(x,y) \in \mathcal{S}} \, dx \, dy.$$  

(31)

The left line passing through the origin at an angle $\theta$ can be given as $y = -x \tan \theta$, while the right line passing through $(\ell,0)$ at an angle $\theta$ can be given as $y = (\ell - x) \tan \theta$. Thus, the BS at $z$ lies in the strip $\mathcal{S}$ if

$$-\infty < y < \infty \quad \text{and} \quad -\frac{y}{\tan \theta} \leq x \leq \ell - \frac{y}{\tan \theta}.$$  

(32)
From (30), (31), and (32), we can express (29) as
\[
E(\Psi[0, \ell] | \theta) = \lambda \int_{y=-\infty}^{\infty} \int_{x=-\infty}^{\infty} \exp(-\frac{\lambda y^2}{\sin^2 \theta}) dx dy
= \ell \left( \sqrt{\lambda} \sin \theta \right).
\]

Since \( \theta \) is uniformly distributed in \([0, \pi]\), averaging over \( \theta \) yields \( E(\Psi[0, \ell]) = \left( \frac{2\sqrt{\lambda}}{\pi} \right) \ell \). Hence, for the case of two beams, the linear intensity of beam reselection is \( 2\sqrt{\lambda} \).

For \( 2^n \) beams with \( n \in \mathbb{N} \), there are \( 2^{n-1} \) possibilities of beam reselections corresponding to the serving BS. In this case, we can obtain the average number of beam reselections by superimposing the beam reselection events corresponding to each beam boundary crossing considered earlier in this proof. Hence, the linear intensity of beam reselection for \( 2^n \) beams at a BS is
\[
\mu_{n,b}(n) = 2^{n-1} \frac{2\sqrt{\lambda}}{\pi} = \frac{2^n\sqrt{\lambda}}{\pi}.
\]

Considering the speed \( v \) of the MT, one gets the time intensity of geometry-based beam reselections as \( \mu_{n,b}(n) \) = \( \frac{2^n\sqrt{\lambda}}{\pi} v \).

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