PillarSegNet: Pillar-based Semantic Grid Map Estimation using Sparse LiDAR Data

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Abstract—Semantic understanding of the surrounding environment is essential for automated vehicles. The recent publication of the SemanticKITTI dataset stimulates the research on semantic segmentation of LiDAR point clouds in urban scenarios. While most existing approaches predict sparse point-wise semantic classes for the sparse input LiDAR scan, we propose PillarSegNet to be able to output a dense semantic grid map. In contrast to a previously proposed grid map method, PillarSegNet uses PointNet to learn features directly from the 3D point cloud and then conducts 2D semantic segmentation in the top view. To train and evaluate our approach, we use both sparse and dense ground truth, where the dense ground truth is obtained from multiple superimposed scans. Experimental results on the SemanticKITTI dataset show that PillarSegNet achieves a performance gain of about 10% mIoU over the state-of-the-art grid map method.

I. INTRODUCTION

Understanding the surroundings perceived by multiple onboarding sensors is crucial in many autonomous systems such as automated vehicles. To achieve reliable scene understanding, automated vehicles are typically equipped with complementary sensors such as cameras, LiDARs, and radars. As one of the key tasks in scene understanding, semantic segmentation associates each pixel of an image or point in a LiDAR point cloud with a semantic class. While image-based semantic segmentation has been well studied, less research in semantic segmentation of LiDAR point clouds has been conducted due to the lack of publicly available datasets for this task. To close this gap, SemanticKITTI \cite{1} has recently been published as the first large-scale dataset for semantic scene understanding using LiDAR. In contrast to conventional camera images, LiDAR point clouds provide more precise distance measurements of the 3D world and preserve the geometric information of objects, empowering a better understanding of the 3D surroundings.

While most existing approaches \cite{2}, \cite{3}, \cite{4} predict point-wise semantic scores from the sparse LiDAR point cloud, Bieder et al. \cite{5} transform the sparse LiDAR point cloud into a multi-layer grid map representation to obtain a dense top-view segmentation of the LiDAR measurements. In Fig. 1, we exemplarily show a semantically annotated 3D point cloud and a corresponding dense top-view segmentation result. We note that such a dense semantic grid map representation is valuable information for subsequent processing in automated vehicles. In particular, as an advancement of conventional occupancy grid maps, it can be advantageous to further distinguish free-space areas such as road, sidewalk, or terrain, and occupied areas such as parked vehicles, buildings, or vegetation.

Since the hand-crafted grid map feature extraction in \cite{5} can result in a potential information loss, we propose to use PointNet \cite{6} to learn features directly from the point cloud and avoid this potential information loss. In this paper, we propose a novel end-to-end method named PillarSegNet to approach dense semantic grid map estimation using sparse LiDAR data. PillarSegNet takes a sparse single sweep LiDAR point cloud as input and subdivides it into a set of pillars in the ground plane. The raw point data in the generated pillars is then fed into a simplified PointNet to extract pillar-wise features, which are scattered back into the top view and form a pseudo image. This pseudo image is then further consumed...
by a modified U-Net to predict a dense semantic grid map. We train and evaluate PillarSegNet on the SemanticKITTI dataset. To this end, we not only transform the point-wise labels in a single sweep into sparse ground truth represented by 2D grid map, but also accumulate multiple neighbouring labelled scans to obtain dense ground truth. The dense labels enables a proper evaluation of the dense prediction produced by PillarSegNet. In addition to the learned pillar features, we further study the benefit of fusing occupancy information obtained via ray-casting. Experimental results show that our approach outperforms the state-of-the-art grid map method by a significant margin in term of mIoU.

In summary, the main contributions of our work are:

1) We propose a novel end-to-end approach to be able to output a semantic grid map given a sparse single LiDAR sweep.

2) We conduct experiments and quantitative comparisons on the SemanticKITTI dataset to prove the effectiveness of our approach.

3) We perform a comprehensive analysis on the semantic segmentation performance using different feature inputs and data augmentation techniques through an ablation study.

II. RELATED WORK

A. Point Cloud Representation

3D LiDAR point clouds are unstructured, irregular and sparse, making it challenging to process them. In the domain of automated driving, it is common to represent 3D point clouds in the top view. Such representation has several advantages including scale invariance and minimal occlusions. To obtain a top-view representation, there are two main groups of methods: grid mapping and learning-based methods.

Grid mapping. Grid mapping approaches, first introduced in [7] are widely used in robotics. The commonly used 2D occupancy grid map encodes the occupancy probability for each evenly spaced grid cell on the ground plane. Since the mapping of 3D measurements to 2D implies a loss of information in the height, [8] further divides the 3D world into a set of 3D voxels and encodes the occupancy information for each voxel to obtain 3D occupancy grid maps. In addition to occupancy, other features such as intensity, density and observations can also be derived to form multi-layer grid maps [9]. In contrast to irregular point sets, the image-like data structure of grid maps enables the use of powerful convolutional operations in deep learning. Therefore, grid maps are utilized in variety of machine learning applications, e.g. object detection [9] and motion estimation [10]. Despite being computationally efficient, grip mapping suffers from an information bottleneck due to the hand-crafted feature extraction, generally leading to a suboptimal performance. For instance, the detection performance for small objects such as pedestrians is noticeably limited in [9].

Learning-based. Since the introduction of PointNet [6], learning-based methods have emerged as prominent alternatives for hand-crafted feature engineering. PointNet is an end-to-end neural network that learns point-wise features from the input point set, demonstrating impressive results on indoor 3D object classification and semantic segmentation. VoxelNet [11] partitions the point cloud into equally spaced voxels and adopts PointNet in novel voxel feature encoding (VFE) layers to learn voxel-wise features. The obtained features are then processed with 3D and 2D convolutions for object detection. PointPillars [12] improves the inference speed by discretizing the point cloud into a set of pillars so that the 3D convolution can be eliminated. Pillar features are further used in different perception tasks, e.g. sensor fusion [13] and ground plane estimation [14], showing promising results. In this paper, we exploit pillar features for semantic grid map estimation. Although PointNet is able to encode point cloud features very well, we note that occupancy features cannot be learned from the data, as they are obtained via ray-casting and employ an inverse sensor model. Thus, we optionally use occupancy features to enrich the point cloud features for a better performance.

B. Image Semantic Segmentation

Image-based semantic segmentation networks are widely used in autonomous vehicles and significant progress is being made in that field. As a pioneering work, FCN [15] adopts fully convolutional layers and stacks them in an encoder-decoder fashion with skip connections, enabling the combination of coarse and fine features at different levels. U-Net [16] builds upon the concept of FCN but uses a larger number of feature channels allowing the propagation of context information to higher resolution layers. The family of DeepLab [17] uses atrous convolutions and atrous spatial pyramid pooling modules to enlarge field-of-views and improve the contextual understanding. In this work, we use a modified U-Net by removing the input convolution block as a trade-off between efficiency and performance.

C. Point Cloud Semantic Segmentation

For point-wise segmentation of LiDAR data, many approaches map the point cloud onto a top-view image in order to benefit from the progress made in image semantic segmentation. RangeNet++ [2] transforms the input point sets into spherical images and uses 2D convolutions for semantic segmentation. Triess et al. [3] propose a scan unfolding method and a cyclic padding mechanism to reduce systematic point occlusions during the spherical projection in [2]. Instead of using range images, GnDNet [14] encodes features in grid-based representation using PointNet for segmenting the ground points. In a recent work, Bieder et al. [5] transform 3D LiDAR data into a multi-layer grid map representation to approach an efficient dense top-view segmentation of point clouds. Nevertheless, it suffers from information loss when generating grid maps and thus performs poor on small objects.

III. METHOD

An overview of the PillarSegNet pipeline is presented in Fig. 2. PillarSegNet takes a sparse single-sweep 3D point cloud as input and predicts a dense semantic grid map in the top view. It consists of two main blocks, a point cloud feature
encoding using parallel pillar and occupancy networks, and a dense semantic segmentation using an encoder-decoder network. The details of each block will be presented in the following sections.

A. Point Cloud Feature Encoding

In the SemanticKITTI dataset, each LiDAR point in the raw point cloud is represented by \((x, y, z, r)\), where \(x\), \(y\), and \(z\) are the 3D coordinates and \(r\) indicates the reflectance. In this work, we consider two kinds of feature encodings obtained from the point cloud: pillar features and occupancy features.

Pillar Features. To learn pillar features, the input point cloud is first discretized into a set of pillars in the ground plane, where pillar is a special voxel without an extension bound in the \(z\) axis. For each LiDAR point with \((x, y, z, r)\) encoding in pillars, we follow PointPillars [12] to further augment it with its offsets from the arithmetic mean \((\Delta x_c, \Delta y_c, \Delta z_c)\) of all points in the pillar and its offsets from the pillar center \((\Delta x_p, \Delta y_p, \Delta z_p)\). The dimension of the resulting point encoding thus becomes \(D = 10\). We predefine the number of pillars per point cloud \((P)\) and the number of points per pillar \((N)\) to create an input tensor of fixed size \((P, N, D)\). To this end, we randomly sample the points if a pillar has more than \(N\) points, or apply zero padding to populate the tensor when a point cloud has less than \(P\) pillars or a pillar has too few points.

Each point in pillars is then consumed by a simplified PointNet that consists of a linear layer, BatchNorm and ReLU, outputting a tensor of size \((P, N, C)\). Then, a max operation along the \(N\) axis is applied to create an output tensor of size \((P, C)\), where each pillar-wise feature is represented by a tensor of size \((C)\). Finally, all pillar-wise features are scattered back to the pillar locations to create a top-view representation of size \((W, H, C)\), where \(W\) and \(H\) denote the width and height of the grid, corresponding to \(x\) and \(y\) direction, respectively.

Occupancy Features. During the measurement process, the detected LiDAR points are the result of a physical ray-casting. When representing the LiDAR points using pillar features, one fundamentally neglects the hidden model information of observability, including information on free space and occupied areas [8]. However, we argue that the observability information might be beneficial for the dense top-view segmentation. Hence, we further extract occupancy features and consider to incorporate them in an additional input stream.

In this paper, the grid map framework in [5] is adopted to generate a single-channel observability map, which indicates the number of transmissions in a grid cell. The observability map is able to represent occupancy information in the 2D grid. We further apply a \(3 \times 3\) convolutional layer on it to learn 2D occupancy features of size \((W, H, Q)\). Considering the possible information loss in the height during grid mapping, we also discretize the point cloud into a 3D voxel grid and encode the occupancy probability for each 3D voxel through ray-casting and voxel traversal [18]. In this way, we get a multi-channel map which represents 3D occupancy information and use it to replace the observability map. Similarly, the voxel map is convolved by \(3 \times 3\) filters to create 3D occupancy features of size \((W, H, Q)\).

Feature Aggregation. We adopt the concatenation operation to aggregate pillar features and occupancy features from the two input streams. The concatenation operation is simple yet effective for fusing different features [13]. After concatenation, we obtain aggregated point cloud features of size \((W, H, C + Q)\).

B. Dense Semantic Segmentation

To obtain the dense semantic segmentation of the input point cloud features, we use an encoder-decoder network, followed by a segmentation head.

Encoder–Decoder Network. In this work, we use a modified U-Net which has an encoder-decoder architecture for feature extraction [16]. The encoder module gradually halves
the spatial size of feature maps and captures higher semantic information, while the decoder module gradually upsamples feature maps and recovers the spatial information. U-Net also introduces skip connections between the aforementioned modules to combine semantic and spatial information. We modify the vanilla U-Net by removing the input convolution block since the aggregated input point cloud features already correspond to a high dimensional feature space. This reduces computational and memory overhead with a negligible loss of performance.

**Segmentation Head.** After the encoder-decoder network, a set of $1 \times 1$ convolutions is performed in the segmentation head to output logits for the classes in the training data. During inference, a softmax function is applied over the unbounded logits to provide softmax probabilities for each grid cell.

**Loss Function.** Due to the heavy class imbalance in the SemanticKITTI dataset, we adopt the weighted cross entropy loss to optimize the model. The weights for the classes are defined by considering the class distribution of the ground truth. The weighted cross entropy loss can be calculated as:

$$
\mathcal{L}_{\text{seg}} = -\frac{1}{M} \sum_{i=1}^{M} (\lambda y_i \log \hat{y}_i + (1-\lambda)(1-y_i)\log(1-\hat{y}_i)),
$$

where $y_i$ and $\hat{y}_i$, respectively, denote the label and softmax probability for pixel i, $\lambda$ is the class-specific weighting coefficient, and $M$ indicates the total number of labeled pixels in the ground truth map. We choose a coefficient of 2 for class *vehicle* and 8 for classes *pedestrian, two-wheel* and *rider*, when utilizing the sparse ground truth for training. When the dense ground truth is adopted, the coefficient for class *vehicle* is modified to 5. The default coefficients for the remaining classes are set to 1.

### IV. Training and Experiments

In this section, we introduce the dataset used to train and validate our approach together with the experimental setup.

**A. Dataset**

We evaluate our approach on the SemanticKITTI dataset [1], [19], which is based on a subset of the KITTI odometry dataset sequences, and contains accurate pose information and semantic labels for each LiDAR point. As in [1], [5], we use sequences 00-07 and 09-10 for training and sequence 08 for validation. In this case, the training and validation sets contain 19130 and 4071 LiDAR scans, respectively. To tackle the under-representation of rare classes, we apply the same merging of 19 into 12 classes as in [5], which also enables a fair comparison. In particular, we map the classes *car, truck and other-vehicle* to *vehicle*, the classes *motorcyclist and bicyclist* to *rider*, the classes *bicycle* and *motorcycle* to *two-wheel*, the classes *traffic-sign, pole and fence* to *object*, and the classes *other-ground* and *parking* to *other-ground*. All *unlabeled* pixels are not considered when optimizing the model.

**B. Ground Truth Generation**

**Sparse Ground Truth Generation.** To obtain the top-view sparse ground truth, we first rasterize a point-wise labelled point cloud into grid cells. For each grid cell, we count the number of points for each of the 12 classes. The semantic class $k_i$ for grid cell $i$ is then determined through a weighted $\text{argmax}$ operation:

$$
k_i = \text{argmax}_{k \in [1,K]} (w_k n_{i,k}),
$$

where $K$ is the number of classes, $n_{i,k}$ denotes the number of points of class $k$ inside grid cell $i$, and $w_k$ is the weighting factor for class $k$. For traffic participant classes including *vehicle, person, rider and two-wheel*, we choose a factor of 5. To ignore the class *unlabeled*, we set the corresponding factor to 0. For all remaining classes, we use a factor of 1. Grid cells without any assigned points are labeled as *unlabeled*. An example of a sparse ground truth map is depicted in Fig. 1.

**Dense Ground Truth Generation** SemanticKITTI contains consecutive LiDAR scans with accurate pose information, which allows the generation of dense ground truth by superimposing multiple labeled scans. For each scan of a sequence, we first collect a set of neighbouring point clouds with a sensor distance $|\Delta p_s|$ smaller than twice the farthest point distance $d$, while limiting the maximal amount of scans to 40. With the provided poses, the selected point clouds are then transformed to the LiDAR coordinate system of the current scan. To avoid aliasing of moving objects during aggregation, we only aggregate points that belong to static objects. For moving objects, we only use information from the current scan. We follow the process used for sparse ground truth generation to create dense ground truth maps. An example of a dense ground truth map is shown in Fig. 1.

**C. Implementation Details**

PillarSegNet takes a sparse single LiDAR sweep as input and outputs semantic probabilities for the 12 classes described in Section IV-A. We implement PillarSegNet based on the OpenPCDet codebase\(^1\). For all experiments, we crop the input point cloud at $([-50, 50), (-25, 25), (-2.5, 1.5)]$ meters along $x$, $y$, $z$ axes respectively. When generating pillars, we use a pillar grid size of $0.1^2 \text{m}^2$, number of pillars $P = 30000$, and number of points per pillar $N = 20$. The channels of the pillar-wise feature learned by PointNet is defined as $C = 64$. The grid cell for generating the observability map and the voxel for encoding the 3D occupancy map have the same $xy$ resolution as the pillar, while the voxel has a $z$ resolution of 0.2 meters. The occupancy features after convolutions have $Q = 16$ channels.

During training, multiple data augmentation techniques, namely *random flip, random rotation, random scaling* and *random translation*, are applied to prevent the network from overfitting on the training data. In *random flip*, every LiDAR point is flipped along the $x$ or $y$ axis by a 50% chance. *Random rotation* means that we rotate every point around the upright $z$ axis by an uniformly distributed angle between

\(^{1}\)https://github.com/open-mmlab/OpenPCDet
The IoU for class $k$, or Jaccard index, is calculated by

$$\text{IoU}_k = \frac{TP_k}{TP_k + FP_k + FN_k},$$

where $TP_k$, $FP_k$, and $FN_k$, respectively, correspond to the number of true positive, false positive, and false negative predictions.

To assess the overall performance, we compute the mean IoU (mIoU) by

$$\text{mIoU} = \frac{1}{K} \sum_{k=1}^{K} \text{IoU}_k.$$  

**Experimental Results.** We train the network in two modes, namely Sparse Train and Dense Train, according to which ground truth is used. The former considers the sparse ground truth, which is obtained from single sweep, whereas the latter considers the dense ground truth, which is obtained by aggregating multiple sweeps. For each experiment using Sparse Train mode, we use two approaches for evaluation: Sparse Eval and Dense Eval, in order to achieve a fair comparisons with the method in [5]. The former considers the sparse ground truth for metrics calculation, whereas the latter considers the dense ground truth, and additionally filters the predictions with the observability map to exclude occluded areas. Note that we only evaluate the Dense Train experiments by the Dense Eval approach.

The experimental results on the full validation set are presented in Table I. We first focus on the results obtained in the Sparse Train mode. Our pillar-based method outperforms the state-of-the-art grid map method [5] by 15.3% and 5.7% mIoU in Sparse Eval and Dense Eval, respectively. In particular, our method achieves a large IoU improvement over the dense ground truth and additionally filters the predictions with the observability map to exclude occluded areas. Note that we only evaluate the Dense Train experiments by the Dense Eval approach.

In addition to pillar features, we further analyse the role of 2D and 3D occupancy features in semantic grid map estimation. By aggregating respective occupancy features, our method achieves an additional improvement in terms of mIoU performance, where the 3D variant performs slightly better when compared with the 2D variant. This demonstrates that the observability information, generated via model-based ray-casting, can be successfully used to further improve the performance of semantic grid map estimation.

We now consider the results obtained in the Dense Train mode. When compared with the Sparse Train mode, training the network on the dense ground truth leads to notable IoU improvements for all classes. For the deployment of semantic grid map estimation, it is thus advisable to leverage dense labels for better performance. Consistent with our previous observation, 2D and 3D occupancy information yield close overall performance gains. Considering the increased computational overhead when generating the 3D occupancy map, it is more practical to aggregate 2D occupancy features and pillar features as a compromise between performance and computational efficiency.

**Inference Time.** We measure the inference time of PillarSegNet on a desktop computer with an Intel i9 CPU and a Nvidia 2080 Ti GPU. Our pillar-based approach achieves a
Fig. 3: Qualitative results produced by Bieder et al. [5] and our approach on the SemanticKITTI validation set. Our network is solely based on the Pillar input features and was trained on the dense ground truth. From top to bottom in each column, we depict the input point cloud, the observability map, the prediction from [5], the prediction from our approach, as well as the corresponding ground truth. The unobservable areas in each prediction map were filtered out according to the observability map. In comparison with [5], our approach shows more accurate prediction on vehicles (cases A & B) and small objects, e.g. two-wheels (cases B & C), Best viewed digitally with zoom.

total runtime of 58 ms. When incorporating 2D occupancy features, additional 10 ms and 6 ms are needed for grid mapping and in the network, respectively.

Ablation Study. We perform thorough ablation experiments to investigate the effect of different data augmentation techniques in our method. The results are reported in Table II. Baseline denotes the method that takes pillar features as input and is trained on the sparse ground truth without any data augmentations. All experiments are evaluated in the Sparse Eval mode. We observe that random flip and random rotation significantly boost the performance with 4.6% gain in terms of mIoU, while random scale contributes to another 0.6% improvement. Unexpectedly, random translation has a negative effect on the overall performance, presumably, because it violates the condition that the ego car should always be in the grid center.

B. Qualitative Analysis

In Fig. 3, we show qualitative results obtained from the approach proposed by Bieder et al. [5] as well as our approach which is based on the Pillar features and was trained on the dense labels. In comparison with the dense ground truth, our approach accurately segments general road scenes, which
include the static environment and varying traffic participants. This demonstrates the ability of our approach for semantic scene understanding from a sparse single LiDAR scan. For instance, when compared with the grid map method, our approach shows more accurate prediction for vehicles (cases A & B) or small objects (cases B & C), indicating the superiority of the learning-based feature extraction.

A video showing qualitative results on the full validation set obtained by our approach is available at: [https://youtu.be/3yidrXBnfo4](https://youtu.be/3yidrXBnfo4).

VI. CONCLUSION

In this work, we presented a novel end-to-end approach named PillarSegNet for semantic grid map estimation based on sparse LiDAR data. PillarSegNet learns features directly from the 3D point cloud, aiming to avoid the information bottleneck caused by hand-crafted feature engineering. Experimental results on the SemanticKITTI dataset show that PillarSegNet outperforms the state-of-the-art grid map method by a large margin in terms of mIoU. We further incorporate occupancy information obtained via ray-casting to enhance the overall performance and identify the 2D occupancy information as the best trade-off between performance and computational efficiency.

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