Location of gap nodes in the organic superconductors \(\kappa-(ET)_2\text{Cu(NCS)}_2\) and \(\kappa-(ET)_2\text{Cu[N(CN)}_2\text{]Br}\) determined by magnetocalorimetry

L. Malone,\(^1\) O.J. Taylor,\(^1\) J.A. Schlueter,\(^2\) and A. Carrington\(^1\)

\(^1\)H. H. Wills Physics Laboratory, University of Bristol, Tyndall Avenue, Bristol, UK.
\(^2\)Materials Science Division, Argonne National Laboratory, Argonne, Illinois 60439, USA.
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We report specific heat measurements of the organic superconductors \(\kappa-(ET)_2\text{Cu(NCS)}_2\) and \(\kappa-(ET)_2\text{Cu[N(CN)}_2\text{]Br}\). When the magnetic field is rotated in the highly conducting plane at low temperature (\(T \approx 0.4\) K), we observe clear oscillations of specific heat which have a strong fourfold component. The observed strong field and temperature dependence of this fourfold component identifies it as originating from nodes in the superconducting energy gap which point along the in-plane crystal axes (\(d_{xy}\) symmetry).

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I. INTRODUCTION

The organic charge transfer salts with general formula \(\kappa-(ET)_2X\) [where ET stands for bis(ethylenedithio)-tetrathiafulvalene] have attracted considerable interest because of their unconventional properties.\(^1\) Like the high-\(T_c\) cuprates this family of quasi-two-dimensional materials exhibit a low temperature superconducting ground state which is in close proximity to an antiferromagnetically ordered Mott insulating state. The position of the various members of the series in the phase diagram is determined by the ‘chemical pressure’ exerted by the anion X. There is considerable evidence that the superconductivity is unconventional.\(^2\) Power-law temperature dependencies observed in thermal conductivity\(^3\) NMR\(^4\) magnetic penetration depth\(^5\) and recently specific heat measurements\(^6\) point strongly to there being nodes in the superconducting energy gap in certain directions of \(k\)-space. In order to gain a better insight into the mechanism for the superconductivity it is important to known the location of these nodes.

The two most widely studied organic superconductors are \(\kappa-(ET)_2\text{Cu(NCS)}_2\) and \(\kappa-(ET)_2\text{Cu[N(CN)}_2\text{]Br}\) (which we abbreviate to \(\kappa\text{-NCS and } \kappa\text{-Br respectively}) as these have the highest superconducting transition temperatures (\(T_c\) of \(\sim 9.5\) K and \(\sim 12.5\) K respectively) at ambient pressure. Angle dependent magneto-thermal conductivity\(^6\) measurements indicate that in \(\kappa\text{-NCS the gap symmetry is } d_{x^2−y^2} (i.e., with nodes at 45° to crystal axis). This conclusion is also supported by an additional tunnelling measurements\(^6\) however it is at odds with most theories of superconductivity such as that of Schmalian\(^6\) based on spin-fluctuation mediated pairing (for a review see Ref.\(^6\)) which predict a \(d_{x^2−y^2}\) pairing state (i.e., with nodes along the crystal axes). In this case the nodes are in the same location, with respect to the dominant nearest neighbor antiferromagnetic coupling direction, as in the high \(T_c\) cuprates. However, Kuroki et al.\(^7\) calculate that a \(d_{x^2−y^2}\) pairing state is often close in energy to the \(d_{xy}\) and can dominate for certain model parameter values.

Here we report an investigation of the location of the nodes in the order parameter of both \(\kappa\text{-NCS and } \kappa\text{-Br using angle dependent magnetocalorimetry as a probe. The magnetic field was rotated in the highly conducting plane of the sample and oscillations of the specific heat were observed. The location of the maxima and minima of the fourfold component of these oscillations points to the order parameter having } d_{xy} \text{ symmetry. This appears to contradict the thermal conductivity results but recent sophisticated theories of magneto-oscillatory specific heat and thermal conductivity predict rather complicated phase diagrams, with the phase of the oscillations with respect to the nodes changing in distinct regions of field and temperature space. Hence, the interpretation of the experimental data is not straightforward and indeed these two seemingly opposite conclusions are not necessarily incompatible.}

Angle dependent magneto-specific heat oscillations were first used successfully to locate the minima in the superconducting energy gap of \(\text{YNi}_2\text{B}_2\text{C}\).\(^12\) Subsequently, experiments were performed in several heavy fermion superconductors: \(\text{Sr}_3\text{RuO}_4\),\(^12\) \(\text{CeCoIn}_5\),\(^13\) \(\text{CeIrIn}_5\),\(^14\) \(\text{PrOs}_4\text{Sb}_12\) and \(\text{URu}_2\text{Si}_2\)\(^15\) as well as the strongly anisotropic s-wave superconductor \(\text{CeRu}_2\).\(^15\) In the simplest case, the oscillations arise from the field induced ‘Doppler’ shift of the energies of the quasiparticle states\(^16\) \(\delta E \propto v_s \cdot \mathbf{k}\), where \(v_s\) is the velocity of the screening currents (\(\propto H\)) and \(\mathbf{k}\) is the quasiparticle momentum. Close to a node or deep gap minimum, this field induced shift can cause a substantial change in the population of the quasiparticle energy levels. In the case of a simple two dimensional d-wave superconductor, if the field is applied along a node then only two nodes will contribute to the change in the density of states as the field is perpendicular to the other two. However, if the field is applied at 45° to this direction all four nodes will contribute, leading to an increase in the angle averaged density of states. Hence, at sufficiently low temperature and field, the direction of the maxima in the density of states should indicate the antinodal directions.\(^17\) Although several experimental quantities are sensitive to these oscillations, the specific heat is perhaps the most direct and
simplest to interpret. For example, to interpret the oscillations in the thermal conductivity, scattering of the quasiparticles from the vortex lattice needs to be taken into account.\textsuperscript{17}

II. EXPERIMENTAL DETAILS

Our samples were grown using a standard electrochemical method\textsuperscript{22} and weighed \(\sim 500\,\mu\text{g}\). The crystal orientation was determined by x-ray diffraction. Specific heat was measured using a purpose built calorimeter based on a bare chip Cernox\textsuperscript{19} thin film resistor. The samples were cooled slowly (\(\sim 0.2\,\text{K/min}\)) to avoid any stress induced phase separation.\textsuperscript{20} The Cernox was used as both heater and thermometer. Two different methods of measurement were used. To measure the temperature dependence of \(C\) the long-relaxation technique was used.\textsuperscript{5,21} For the rotation studies, where much smaller temperature excursions from the base temperature are required, a thermal modulation technique was used.\textsuperscript{22,23} An ac current \((\omega \simeq 3-6\,\text{Hz})\) was passed through the Cernox and the signals at \(\omega\) and \(3\omega\) detected with lock-in amplifiers. The \(3\omega\) signal is inversely proportional to the specific heat provided that \(\omega\) is selected appropriately.\textsuperscript{22,23} The thermometers were calibrated in field using a \(^3\text{He}\) vapor pressure thermometer (below 4 K) and a capacitance thermometer at higher temperature. The angle dependence of the thermometer magnetoresistance was measured directly, and was found to be negligibly small. Any angle dependence of the addenda specific heat was checked by measuring a pure Ag sample at our base temperature and in fields up to 14 T. No change was detected to within a precision of 0.2%. The thermal modulation method has the advantage of high resolution at the expense of a small (\(\sim 10\%\)) systematic error in the absolute values.

For measurements as a function of field angle the calorimeter was mounted on a mechanical rotator whose rotation plane was parallel to the field. Sample alignment was done by eye and was checked using optical images. Using this arrangement we estimate that the field was kept parallel to planes to within a few (\(\lesssim 5\)) degrees. Experiments were done either by rotating the sample at low temperature or by heating the sample above \(T_c\) after each rotation. In general, the two methods gave very similar results however there were occasional reproducible jumps in the data in certain field directions when the sample was not heated above \(T_c\) after each rotation, presumably because of vortex pinning effects.

III. RESULTS AND DISCUSSION

For \(B^\perp = 14\,\text{T}\) (applied along the interlayer direction) both samples are in the normal state and the data follow \(C/T = \gamma + \beta_3 T^2 + \beta_5 T^4\), with \(\gamma = 29 \pm 1\,\text{mJK}^{-2}\text{mol}^{-1}\) for \(\kappa\text{-Br}\) and \(33 \pm 1\,\text{mJK}^{-2}\text{mol}^{-1}\) for \(\kappa\text{-NCS}\) in good agreement with previous measurements.\textsuperscript{2} We do not observe any Schottky-like upturns even at high field, so the \(\kappa\text{-Br}=14\,\text{T}\) data is likely to be very close to the normal state \(C\) at zero field.\textsuperscript{2} The zero field data with the 14 T data subtracted shown in Fig. 1 shows the superconducting anomalies of each sample with midpoints at 9.6 K and 12.5 K for \(\kappa\text{-NCS}\) and \(\kappa\text{-Br}\) respectively.

We now discuss the data with the field rotating in the basal plane. Fig. 2 shows the raw \(C(\phi)\) data for \(\kappa\text{-Br}\) at several temperatures and \(B^\perp=3\,\text{T}\) which is \(\sim 10\%\) of \(H_c2\) for this field orientation.\textsuperscript{25} \(\phi\) is the angle measured relative to the in-plane \(c\)-axis. Focusing on the lowest temperature data \(T=0.4\,\text{K}\), we see that the total change in \(C\) with angle is around 33\% of the total (minus addenda) or around 55\% of the electronic term at this field (the phonon contribution at \(T=0.4\,\text{K}\) and \(\kappa\text{-NCS}\) which is 60\% of the total). The largest component has twofold symmetry, however to get a good fit we need also to include a fourfold term. We find the data are best fitted by the function

\[
C(\phi) = C_0 + |C_2 \cos(\phi + \delta_2)| + C_4 \cos(4\phi + \delta_4)
\]

which fits the data perfectly within the noise as shown by the residuals displayed in the figure. The fit parameters are \(C_2 = 0.54\,\text{mJ}\,\text{mol}^{-1}\text{K}^{-1}\), \(\delta_2 = 13 \pm 2^\circ\), \(C_4 = 0.04\,\text{mJ}\,\text{mol}^{-1}\text{K}^{-1}\), and \(\delta_4 = 0 \pm 2^\circ\).

The \(C_2\) two-fold term likely originates from a combination of sample misalignment and the anisotropy of the Fermi surface of these compounds. If the sample is misaligned by an angle \(\phi\) to the plane of rotation, then there will be a component of magnetic field \(B^\perp\) perpendicular to the planes given by \(B^\perp/B_0 = \cos \phi \sin \varphi\), where \(B_0\) is the applied field and \(\varphi\) is the in-plane rotation angle. As
fields $\Delta C(B) \sim (B/B_2)^{1/2}$, however in general the functional dependence may not be a square root (for example if the field is less than a scale set by the impurity scattering bandwidth then $\Delta C \sim -B/B_2 \ln(B/B_2)$ Ref. 28). Experimentally, for these compounds for $B \perp \gtrsim 0.1$ T $\Delta C(B)$ is close to linear. Given that this misalignment term must be even with respect to $B$, the simplest form is then $\Delta C(\phi) = A|\sin(\phi + \delta)|$, where $A$ is constant which depends on the misalignment angle and the form of the function $F$ and $\delta$ is a constant which depends on the misalignment angle. For simplicity we took $F$ to be a simple power law so the misalignment term is $\Delta C(\phi) = A|\cos(\phi + \delta)|^n$. A least squares fit to the data with this in place of the $C_2$ term in Eq. 1 gives $n = 1.1 \pm 0.1$, so we fixed $n = 1$ for all temperatures and fields.

The crystal structures of $\kappa$-Br and $\kappa$-NCS are orthorhombic and monoclinic respectively. The Fermi surface of $\kappa$-NCS has been determined by both tight-binding and first-principle calculations and quantum oscillation measurements and is sketched in Fig. 3. The quasi-two-dimensional Fermi surface would have a near ellipsoidal cross-section if all the ET-dimers were equivalent. However, the difference in the inter-dimer hopping integrals causes a gap to appear where the ellipse crosses the Brillouin zone boundary. The Fermi surface of $\kappa$-Br is very similar to that of $\kappa$-NCS except that there are twice the number of Fermi surface sheets because the unit cell contains twice the number of formula units due to the doubling of the $c$-axis.

Theoretical calculations based on spin-fluctuation pairing suggest that the pairing state has either $d_{xy}$ or $d_{x^2-y^2}$ symmetry. For the case of $d_{xy}$ pairing as the gap has nodes along the crystal axes so the angle between these nodes remains 90° even in the presence of the orthorhombic distortion, and maxima in $C(\phi)$ with 4-fold symmetry as in Eq. 1 are expected. In the semiclassical theory the field dependence of the specific heat depends on the Fermi velocity and gradient of the superconducting energy gap $\Delta$ near the nodes $d\Delta/d\phi|_{\text{node}}$. So an orthorhombic distortion of the Fermi surface can produce a two-fold $|\cos \phi|$ dependence of $C(B)$ similar to the case of field misalignment. Indeed, in the field angle dependent thermal conductivity measurements of $\kappa$-NCS a two fold term around two times larger than the four fold term was observed at $T = 0.43$ K (Ref. 6) even though the field was aligned to better than 0.01°.

As the phase of the two-fold term in our measurements implies symmetry far from a crystal symmetry direction, this suggests that a sizeable fraction of it originates from misalignment, however the thermal conductivity results suggest that the intrinsic contribution is not negligible. In principle, in-situ adjustment of the crystal orientation (using for example a vector magnet as in Ref. 6) and angle detection using the magnetoresistance of the sample would allow us to distinguish between these two contributions however this was not possible with our current set-up.

FIG. 2. Color online. Raw data for $\kappa$-Br taken at three temperatures 0.4 K, 0.8 K and 1 K. The blue lines are a fit to a twofold angle dependence whereas the red lines include the additional fourfold term as described in the text.

$H_{c2}$ is much lower for field applied perpendicular rather than parallel to the planes there will be a induced component to $C(\phi)$ which will depend on $B \perp$. For a pure $d$-wave superconductor at low field we would expect that at low

FIG. 3. Color online. Sketch of the Fermi surface of $\kappa$-NCS along with the definition of $\phi$. The red dots show the position of the nodes in for the $d_{xy}$ pairing state.
The solid lines are fits to $C_4 \cos(4\phi + \delta_4)$.

In Fig. 4 we show the $\kappa$-Br data with the twofold term subtracted and normalized to the angle averaged value of the electronic specific heat at the relevant temperature and field $C_e(H,T)$. At $T=0.4$ K the fourfold term is now clearly evident. It has a relatively large peak to peak amplitude of $\sim 7\%$ of $C_e(H,T)$. Note that the in-plane shape of this sample is an irregular polygon and so the fourfold term cannot result from shape dependent vortex pinning effects. The phase of this term is $\delta_4 = 0 \pm 2^\circ$, so that the minima occur when the field is along the $a$ and $c$ crystal axes (equivalent to the $b$ and $c$ axes for $\kappa$-NCS in Fig. 3). Hence, we conclude that the nodes in the gap function are located along the crystal axes, i.e., the energy gap has $d_{xy}$ symmetry.

As the temperature is increased the relative size of the fourfold term compared to the angle average decreases rapidly, and is barely discernable in the $T=1$ K data. This strong decrease with increasing temperature points strongly to the origin of the fourfold oscillation being from nodal quasiparticles, rather than, for example, $v_F$ anisotropy which would have a much weaker $T$ dependence. For CeRu$_2$, which has a strongly anisotropic $s$-wave gap ($\Delta_{\text{max}}/\Delta_{\text{min}} \simeq 5 - 10$), it is found that $C_4/C_e$ increases with increasing $T$ up to a maximum at $T/T_c \simeq 0.16$.\cite{5} Fig. 4 also shows that the magnitude of the fourfold term depends strongly on the applied field. It is maximal at $B=3$ T and is significantly reduced for $B=4$ T and 4 T.

Data for $\kappa$-NCS are also shown in Fig. 4. The magnitude of the fourfold term is comparable to that found for $\kappa$-Br, and importantly the maxima/minima are at the same angles, so we expect the symmetry of the gap functions to be the same. For this sample we had to introduce an additional term $C_1 \cos(\phi + \delta_1)$ which is comparable in magnitude to the $C_2$ term to fully fit the background, the origin of which is unclear. The temperature and field dependence of the fourfold component $C_4$ for both samples is shown in Fig. 5. As for $\kappa$-Br, $C_4/C_e$ in $\kappa$-NCS decreases strongly with increasing temperature and decreasing field. However, for $\kappa$-NCS $C_4/C_e$ decreases significantly less as the field is increased from $B=3$ T to $B=4$ T than in $\kappa$-Br.

In Fig. 5 we compare our experimental data to quantitative predictions of the magnitude of this effect for a $d$-wave superconductor. For simplicity we use the nodal approximation of the Doppler shift theory which gives the following expression for the field/angle dependence of the density of states\cite{15,16,17}

$$N(\omega,H,T) = \frac{1}{2} \left[ F_1 \left( \frac{\omega}{E_1} \right) + F_2 \left( \frac{\omega}{E_2} \right) \right]$$

where the field scale $E_H = 0.5 a v_F \gamma_\lambda^{-\frac{1}{2}} \pi |\mu_0 H/\Phi_0|$, $E_1 = E_H \sin(\pi/4 - \phi)$, $E_2 = E_H \cos(\pi/4 - \phi)$ and

$$F(y) = \begin{cases} y \left[ 1 + 1/(2y^2) \right], & \text{if } y \geq 1, \\ (1 + 2y^2) \arcsin y + 3y \sqrt{1 - y^2} / y, & \text{if } y \leq 1. \end{cases}$$

In this approximation, which was shown to be in good agreement with more sophisticated treatments in the
low temperature/field limit only quasiparticles in the nodal directions are included. This density of states was used to calculate the entropy $S$ then numerically differentiated to give the heat capacity $C = T \partial S / \partial T$. For the curve in the figure we set $E_H = 0.13 \sqrt{\mu_0 H} k_B T_c$.

The theory and experiment show reasonable agreement considering this contains just one fitting parameter $E_H$. In particular, the theory explains the rapid decrease in signal with increasing temperature. For $\kappa$-NCS, using the in-plane Fermi velocity $v_F = 1.1 \times 10^6$ m/s and penetration depth anisotropy $\gamma_\lambda \approx 100$, this gives $E_H \approx 0.1 T \sqrt{\mu_0 H} k_B T_c$ (setting the numerical constant $a = 1$). This agreement with the experimental value is probably fortuitous as $a$ and the effective value of $\gamma_\lambda$ depend on the details of the vortex lattice. The increase in field between 2 and 3 T is similar to that predicted by the theory but does not explain the observed decrease in higher field. However, more sophisticated treatment actually predict that the oscillations in $C$ change sign for $T \gtrsim 0.1 T_c$ or for $H \gtrsim (0.2 - 0.4) H_{c2}$ and so a strong decrease of $C_4$ with increasing field is expected near these transition points.

IV. CONCLUSIONS

In summary, the magnetic field angle dependence of the heat capacity of Ce-Br and $\kappa$-NCS shows a clear four-fold oscillation. These oscillations are shown to arise from nodes in the superconducting gap situated along the crystal axis. These results imply a $d_{xy}$ order parameter that is consistent with the spin fluctuation mediated pairing theory of Schmalian and others. At first sight these results seem to contradict the angular thermal conductivity $\kappa$ experiments performed on $\kappa$-NCS which showed that the small fourfold component (\approx 0.1% of the total $\kappa$) was 45° out of phase with the one observed in this experiment (i.e., a maximum of $\kappa$ was observed with the field along the $b$ or $c$ axes whereas a minimum is observed here). A similar discrepancy between the $C$ and $\kappa$ measurements was found for CeCoIn$_5$. Vorontsov et al. have shown that the oscillations in $C$ and $\kappa$ both change sign as a function of $H$ and $T$ and so the CeCoIn$_5$ results could be explained because the measurements of $C$ and $\kappa$ were conducted in different regions of the $(H,T)$ phase diagram. According to the phase diagrams in Ref. our $C$ measurements should be well within the low $(T,H)$ limit so the minima are along the nodal directions. The $\kappa$ measurements were made at similar $H$ and $T$ and also should be in the low $(H,T)$ limit with minima along the nodal directions, however in this case they are much closer to the sign switching phase boundary. Hence the previous thermal conductivity and the present data are not necessarily inconsistent and might be explained if there were small material dependent changes to the global phase diagrams of Ref. Further work will be required to understand this.

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