Single photons exhibit inherently quantum and unintuitive properties such as the Hong-Ou-Mandel effect, demonstrating their bosonic and quantized nature, yet at the same time may correspond to single excitations of spatial or temporal modes with a very complex structure. Those two features are rarely seen together. Here we experimentally demonstrate how the Hong-Ou-Mandel effect can be spectrally-resolved and harnessed to characterize a complex temporal mode of a single-photon – a zero-area pulse – obtained via a resonant interaction of a THz-bandwidth photon with a narrow GHz-wide atomic transition of atomic vapor. The combination of bosonic quantum behavior with bandwidth-mismatched light-atom interaction is of fundamental importance for deeper understanding of both phenomena, as well as their engineering offering applications in characterization of ultrafast transient processes.

Single photons exhibit a plethora of highly nonclassical features manifesting their quantized and bosonic nature and demonstrating the meanders of quantum theory. One of classic examples is the Hong-Ou-Mandel (HOM) effect [1]. When two identical photons enter two respective input ports of a balanced beamsplitter (BS), the photons always leave together via a single output port. In consequence no coincidences between the ports can be observed. This unintuitive feature fundamentally stems from the destructive interference of two-photon amplitudes corresponding to two scenarios each with one of the photons reflected and one transmitted. Interestingly, observing reminiscent coincidences with a single-photon camera (i.e. spatial/angularly resolved) allows one to probe and localize the wavefront differences of the two photons, which has been leveraged to precisely measure a single-photon wavefront in a method reminiscent of classical holography [2]. Two-photon interferograms, measured with either spatial/angular or temporal/spectral resolution, are also at the core of superresolution imaging [3], quantum fingerprinting [4-6] and photon-pair source characterization [7-10]. Spectrally-resolved HOM effect has been measured with a dispersive fiber spectrometer [11, 12]. HOM interference extends beyond the photonic realm and has been shown for other bosonic (quasi)particles such as atoms [13, 14], phonons [15] or spin-waves [16, 17].

The non-classical features of SPs become intriguing when the spatial or temporal mode has a nontrivial structure with added qualitative features such as orbital angular momentum (OAM). In the spatial domain, mode structuring has lead to insights and applications such as remote object identification [18], improved sensitivity [19], and uncertainty relations for OAM [20]. However, with mostly single mode optical architectures, the mode engineering in time-frequency (TF) degree-of-freedom (DoF) attracts most attention, enabling bandwidth matching [21], generating and manipulating high-dimensional entanglement on-chip [22] and studies of global-versus-local two-photon interference (TPI) in quantum networks [23].

SPs exhibit complex light-matter interactions, mostly studied in the classical regime and leading to complex modal structure. One such a case is the resonant interaction of an ultrafast pulse with a slowly relaxing medium e.g. a femtosecond pulse passing through atomic vapor – a case demonstrated to produce zero-area (ZA) or π pulses [24, 25] with temporal envelopes consisting of alternating ± sign lobes. This interaction has been demonstrated for SP states and Rb vapor [26], exploring a vastly unharnessed region of light-matter interaction between a THz-bandwidth photon and a GHz-wide (Doppler broadened) atomic transition. While the photon is rarely absorbed, the interaction is highly dispersive leaving the photon in the ZA temporal shape and imprinting a spectral phase (SPHI). Costanzo et al. [26] characterized SP ZA pulses in the temporal domain via homodyne detection, which is a robust tomography method, yet never provides optimal information due to inherent shot noise. Single-photon holography can directly reconstruct the SPHI resulting from bandwidth-mismatched (BM) light-matter interaction, without local oscillator (LO) optimization and the shot noise contribution inherent to homodyne techniques. Characterizing the SPHI at a single-photon level is of fundamental importance for quantum coherent control techniques [27, 28] and utilization of the TF DOF in quantum networks [29]. High-bandwidth ultrafast photons can also efficiently interact with atomic vapors via two-photon transitions [27, 29]. Furthermore, ultrafast frequency combs have been used to probe temporal dynamics of two-photon transitions via direct frequency comb spectroscopy [30] combining high temporal resolution and a vast spectral range.

In this Letter we combine two highly nonintuitive concepts and demonstrate spectral single-photon holography...
(SSPH) applied to the characterization of ultrafast ZA SP pulses. Idea of our experiment is depicted in Fig. 1. We employ spontaneous parametric down-conversion (SPDC) to produce pairs of SPs – an idler and a signal – with central wavelengths of 795 nm. The signal photon with 10 nm bandwidth passes through a hot Rb vapor, resonantly interacting with the D1-line electronic transition, and obtaining both a ZA temporal shape and intrinsically a nontrivial SPHI profile imprinted through light-matter interaction. The photon pair is then interfered on a BS. The output ports (±) are analyzed with a single-photon spectrometer and coincidences in wavelength coordinates (λ±) are counted. The inset of Fig. 1 depicts a simulated coincidence map. In the absence of the BS and the Rb cell the coincidence map would just be the joint spectral intensity (JSI) of the two-photon state. Notably, if only the Rb was removed, we would ideally see no coincidences at all, indicating the SPHIs of the two-photons are identical. A coincidence pattern uniquely corresponds to a SPHI difference between the photons and carries a footprint of the interaction between a THz-bandwidth photon and a GHz atomic transition.

Fundamentally, our demonstration combines a vastly unexplored regime of bandwidth-mismatched light-matter interaction with a purely quantum effect of TPI. The previous SP ZA pulses demonstration 20 employed temporal homodyne detection requiring LO temporal mode optimization 31. In comparison, SSPH does not require LO or any optimization, working readily for any kind of SPHI profiles. Importantly for quantum metrology, our method also avoids the shot noise inherent to homodyning.

We envisage applications of SSPH for characterization of ultrafast transient phenomena such as chemical reactions or for biological measurements [see supplementary material (SM) 32], which could benefit from negligible absorption of the probe photons. Ultrafast pulses have proved indispensable where time resolution is required e.g. for time-resolved photoemission tomography of molecular orbitals 45, probing the transition states of chemical reactions 16, 17 or their coherent control 15, 49. SSPH can supplement these methods as recent times see more and more proposals for using quantum light 50, 51 and TPI effects in spectroscopy 52. For instance, femtosecond transition state spectroscopy 40, 45, 54 relies on a pair of pump and delayed probe femtosecond pulses. SSPH could replace the typical probe fluorescence signal for a direct noninvasive characterization. SP operation also promises flexibility in molecular control 54 via quantum non-demolition continuous measurements 55 and relying on the TPI and coincidence post-selection, provides robustness to the noise from scattering surroundings of the biological samples.

Our experimental setup consists of a SP source (Fig. 2(a)) and of SSPH part (Fig. 2(b)). To produce ultrashort SP states we employ the type-I noncollinear SPDC process in a beta barium borate (BBO, 2 mm length along optical axis), pumped with a focused pump beam with 397.5 nm central wavelength, Gaussian beam radius of w0 = 70 μm and 100 mW average power. To obtain the blue pump, we employ second harmonic generation of femtosecond pulses (100 fs, central wavelength of 795 nm) from a Ti:Sapphire laser (Spectra-Physics MaiTai), in a second BBO crystal (0.5 mm length along optical axis). The SPDC emission is spectrally filtered with an interference filter (FWHM 10 nm) tilted to have the central transmission wavelength at 796.7 nm. Two Gaussian transverse modes are selected by coupling to single-mode fibers. The modes are chosen for highest correlation and SP brightness. Selected modes, corresponding to signal and idler photons, enter the second part of the setup. Signal photons pass through a heated Rb vapor cell. The cell temperature controls the optical depth [OD, see SM] which determines the strength of light-matter coupling. The photon leaves the Rb cell in an ZA temporal shape and with its SPHI given by a single Lorentzian resonance profile centered on the λ0 = 795 nm D1 Rb line [34].

\[
\varphi_x(\lambda) = \text{OD} \times \frac{x(\lambda)}{1 + x(\lambda)^2},
\]

where \(x(\lambda) = 2\pi c (\lambda - \lambda_0) / \lambda_0^2\) with \(c\) denoting the speed of light and \(\tau\) is the Doppler-broadened lifetime of the excited state ranging from 215 ps to 240 ps for employed Rb temperatures (see SM). The idler photon is delayed.
pulses from Ti:Sapphire laser (central wavelength emission cone. Dichroic mirrors (DM) for tons are spectrally filtered (IF, see main text) and coupled to frequency-doubled in a BBO crystal (BBO-SHG) and used to Figure 2. (a) Source of single-photon pairs. (b) Setup for SSPH. The photons’ polarizations are then jointly rotated on a polarization-based equivalent of a balanced BS, a setup compensated). The photon pair is then interfered on a + (−) region at the λ+ (λ−) coordinate. We subtract accidental coincidences A(λ+,λ−) = n(λ+)|n(λ−)|) to obtain the coincidence map:

\[ C(λ+,λ−) = R(λ+,λ−) - A(λ+,λ−), \]

which is the photon-number covariance. The subtraction is required due to many experiment repetitions per single camera frame, creating artificial coincidences (see SM).

To predict the form of \( C(λ+,λ−) \) we consider the two-photon component of the signal (s) and idler (i) joint wavefunction \( Ψ(λ_s,λ_i) \). The probability of observing a coincidence at spectral coordinates \( λ_± \) of ± BS ports is given by:

\[ P_c(λ_+,λ−) = \frac{1}{4} |Ψ(λ_+,λ−) - Ψ(λ−,λ+)|^2. \]

We assume that the photons are identical except for the SPHI \( Ψ_+(λ) \) of the signal mode i.e. \( Ψ(λ_−,λ+) = Ψ(λ_−,λ+) \exp\{i[ψ_s(λ−) - ψ_s(λ+)])\}. Hence,

\[ P_c(λ_+,λ−) = \frac{1}{2} [1 - \cos(ψ_s(λ+)|−ψ_s(λ−)|)] |Ψ(λ_+,λ−)|^2, \]

where the first term lets us reconstruct the SPHI \( ψ_s(λ) \) and the second corresponds to the JSI of the photon pair. Additional mode mismatch between the photons decreases the interference visibility, corresponding to cos(…) → V cos(…) for visibility \( V \leq 1 \).

The coincidence maps for three Rb cell temperatures \( (T_1 = 188 °C, T_2 = 174 °C, T_3 = 86 °C) \) are presented in Fig. [3] along with theoretical predictions. The fidelity \( 0 \leq F \leq 1 \) between the experimental and theoretical maps normalized to a unit sum, yields 94%, 86%, 89% for \( T_1, T_2 \) and \( T_3 \), respectively. In all maps the coincidences are most strongly present on a broad stripe along the anti-diagonal. This feature stems from JSI \( |Ψ(λ_+,λ−)|^2 \) of the SPDC photon pairs, which in our case are spectrally correlated. See SM for comparison of simulated
Figure 3. Spectral single-photon holograms of an ultrafast 100 fs photon resonantly interacting with Rb vapor heated to (a) $T_1 = 188$ °C, (b) $T_2 = 174$ °C, (c) $T_3 = 86$ °C. Left column represents experimental results i.e., the observed photon number covariance $C(\lambda_+, \lambda_-)$ (coincidences with subtracted background) in spectral coordinates $\lambda - \lambda_0$ between ports of a BS. The BS interferes the measured photon with the reference. Central column corresponds to a theoretical prediction of a spectrally-resolved coincidence probability $P_c(\lambda_+, \lambda_-)$ with no imperfections ($\nu = 1$), as given by Eq. (1). Right column: theoretical prediction for the SPHI $\varphi_s(\lambda_- - \lambda_0)$ modulo $2\pi$, given by Eq. (1).

interferograms with correlated and uncorrelated photons and JSI maps. The characteristic cross at $\lambda_0 = 795$ nm corresponds to the Rb resonance where the phase variation becomes too rapid to be resolved. The coincidences in this region correspond to a phase-averaged case. The phase shift flip around $\lambda_0$, illustrated in the right column of Fig. 3 follows from Eq. (1). While the brief interaction between a SP and Rb atoms has the most pronounced spectral footprint at higher temperatures, corresponding to fitted optical depths of OD($T_1$) = $4.6 \times 10^3$ and OD($T_2$) = $2.6 \times 10^3$, the presence of much cooler Rb at $T_3$ is still distinctly identifiable, despite a comparably low OD($T_3$) ≈ 20 yielding a peak-to-peak SPHI variation of 20 rad. This observation suggests metrological applications in non-disturbing sensing of the sample presence. The OD values corresponding to SPHIs reconstructed from the experimental data are in a good agreement with the theory prediction for independently measured Rb cell temperatures. Even without prior knowledge of the phase profile $\varphi(\lambda)$ standard holographic reconstruction techniques [36, 37] can extract $\varphi(\lambda)$ since the problem is analogous to the processing of classical interferograms. We have verified the Fourier-domain retrieval of $\varphi_s(\lambda_+ - \lambda_-)$ modulo $2\pi$, for the case of $T_1 = 188$ °C (see SM).

The interference visibility in SSPH is not only a benchmark of the setup quality, but estimated locally $\nu(\lambda_+, \lambda_-)$ carries unique information. The total phase $\varphi_s(\lambda_+ - \varphi_s(\lambda_-)$ estimated from the coincidence map is a 2-dimensional abundant representation of a 1-dimensional $\varphi_s(\lambda)$ enhancing estimation of $\varphi_s(\lambda)$ and guaranteeing that the cos term in Eq. (4) cannot be constant over the spectral range of $\varphi_s(\lambda)$ unless equal to unity (in which case $P_c = 0$). Hence, when the local visibility $\nu(\lambda_+, \lambda_-)$ falls to 0 over extended regions with coincidences present $P_c(\lambda_+, \lambda_-) \neq 0$, it is a strong indicator of rapid oscillations below resolution (averaging cos to 0). The method can thus detect presence of spectral features on sub-resolution scales. Finally, we have quantified the visibility by dividing a smoothed version of the experimental coincidence map into square regions (1 nm sidelength) and locally estimating the visibility from the maximal and minimal value within the region. This way we obtained average visibility of $\nu \approx 0.69 \pm 0.16$, $\nu \approx 0.79 \pm 0.12$ and $\nu \approx 0.88 \pm 0.09$ for $T_1 = 188$ °C, $T_2 = 174$ °C and $T_3 = 86$ °C, respectively, where the uncertainties correspond to one standard deviation across the regions. For more details see SM. For comparison, using classical light the maximal attainable visibility of TPI is 50%.

Metrological advantage of SSPH over homodyne detection. In conventional homodyning, we measure a variance of homodyne current of the signal SP. To gain full information, we consider a multi-pixel measurement and analyze covariance (see SM for setup examples), which has been previously considered in the time domain [62]. The homodyne signal is zero-mean with covariance of $\sim [\frac{1}{2} \delta(\lambda_+ - \lambda_-) + |\psi_+(\lambda_+)\psi_-(\lambda_-)| \cos(\varphi_s(\lambda_+) - \varphi_s(\lambda_-))$ with an inherent shot noise component (first term) and $\psi_s(\lambda)$ being the SP wavefunction, which is in contrast to SSPH (Eq. 3). To further elucidate the advantage, consider a more direct scenario of self-guided tomography [63], where spectro-temporal shaping is employed both for a LO and the reference SP. We strive to shape the reference to be the same as the signal photon. The homodyne case involves maximizing the the inherently noisy variance. The SSPH involves minimization of the coincidence count, which becomes a low-noise signal with no offset. This can be directly demonstrated by considering the estimation of residual distinguishability $\alpha \ll 1$ between signal and reference modes, as derived in the SM in the context of Fisher information $F_\alpha$ per experimental shot. We obtain $F_\alpha \sim \alpha^{-1/2}$ for the homodyning and $F_\alpha \sim \alpha^{-1}$ for the SSPH, which unequivocally demonstrates the preferable scaling of the SSPH. With no prior
knowledge ($\alpha \approx 1$) hybrid of homodyning followed by SSPH may be beneficial.

In this Letter we experimentally combined highly unintuitive phenomena bringing together the bosonic and quantum nature of SP light and the complex spectral structure of ultrafast ZA pulses obtained in resonant BM interaction between a SP and $^{87}$Rb vapors. Our experiment demonstrates how the Hong-Ou-Mandel effect can be spectrally resolved and harnessed for characterization of ultrafast SPs in a holography-like method. The broadband ultrafast photons carry a unique spectral footprint of the resonant interaction with narrow atomic transitions, corresponding to their ZA temporal shape. Demonstrated herein, SSPH both supplements and extends previous homodyne measurements of SP ZA pulses, as well as promises unique applications in probing ultrafast transient phenomena such as picosecond-scale chemical reactions. Notably, no matching of the reference to the photon is required. This may on one hand come as a surprise, since visibility of interference is reduced as the two photons cease to match in the time domain. Our method solves this via spectrally-resolved detection, where local visibility of spectral HOM interference is high. Furthermore, it broadens the fundamental understanding of SP BM light-atom interactions and brings closer the prospect of engineering those phenomena for the range of applications. Apart from spectroscopic applications, such interactions may find natural applications in quantum information processing in the spectral domain [64–66].

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