Strain engineered pyrochlore at high pressure

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Strain engineering is a promising method for next-generation materials processing techniques. Here, we use mechanical milling and annealing followed by compression in diamond anvil cell to tailor the intrinsic and extrinsic strain in pyrochlore, Dy2Ti2O7 and Dy2Zr2O7. Raman spectroscopy, X-ray pair distribution function analysis, and X-ray diffraction were used to characterize atomic order over short-, medium-, and long-range spatial scales, respectively, under ambient conditions. Raman spectroscopy and X-ray diffraction were further employed to interrogate the material in situ at high pressure. High-pressure behavior is found to depend on the species and concentration of defects in the sample at ambient conditions. Overall, we show that defects can be engineered to lower the phase transformation onset pressure by ~50% in the ordered pyrochlore Dy2Ti2O7, and lower the phase transformation completion pressure by ~20% in the disordered pyrochlore Dy2Zr2O7. These improvements are achieved without significantly sacrificing mechanical integrity, as characterized by bulk modulus.

Strain engineering is an effective method to manipulate the electronic structure of materials1–5, synthesize new materials6–7, and enhance various properties of nano-scale materials8–9. Multiple methods for introducing strain have been used, including mechanical milling6–7, chemical doping6, substrate patterning6, monolayer buckling6, uniaxial tension6, biaxial compression10, and quasi-hydrostatic compression4, 11. Some of these techniques (e.g., chemical doping and mechanical milling) are considered “intrinsic” since they increase strain without the continuous application of an external force. In contrast, other techniques (e.g., tension and compression) are “extrinsic” since the strain they apply is reliant on the continued application of said external force. Thus, intrinsic and extrinsic methods of strain engineering can be used in conjunction to further take advantage of the material modifications they induce.

The combination of mechanical milling, which has been shown to greatly affect the kinetics of phase transformations4, and quasi-hydrostatic compression by diamond anvil cell (DAC), which controls a fundamental thermodynamic parameter, pressure, provide two separate methods of controlling strain in materials. Mechanical milling followed by annealing provides a means to synthesize materials with varying amounts of intrinsic strain, while compression by DAC extrinsically increases strain in the material. Here, we have investigated the behavior of Dy2Ti2O7 and Dy2Zr2O7 pyrochlore oxides prepared by mechanical milling and subsequent annealing (to control defect concentration) under high-pressure conditions in a DAC. DACs allow materials to be studied in situ at high pressure, providing the ability to gain a fundamental understanding of material behavior. This understanding can then lead to the optimization of other high-pressure processing techniques that can be applied to large volumes of material12–14.

Pyrochlore (A2B2O7) complex oxides have shown utility in a wide range of technological applications. They have been proposed as nuclear waste forms for the immobilization of actinides15, electrolytes for solid oxide fuel cells8, 16, and quantum spin ices17. The behavior of defects in pyrochlore is important for many of these applications. As such, multiple methods for introducing defects into pyrochlore have been investigated in the past, including radiation damage18–21, high pressure22–24, and chemical doping25–27. A thorough understanding of the pyrochlore crystal structure is necessary to assess the behavior of defects in the material, and how those atomic-level defects can influence bulk properties. The intricate structure of pyrochlore oxides—with two cations that may or may not be ordered and coupling between the character of the cation and anion sub-lattices—also makes it an ideal candidate to study defects in from the perspective of fundamental science.
The ordered pyrochlore structure ($Fd-3m$) is a derivative of the AX$_2$ fluorite structure ($Fm-3m$). Pyrochlore-structured materials have two distinct cation sites, as opposed to the ideal fluorite structure that has only one. Furthermore, 1/8 of the fluoride anion sites are vacant in the pyrochlore structure. These systematic vacancies are ordered, and they occupy a distinct site in the pyrochlore structure. The ordered pyrochlore structure forms when the ratio of the A and B cation radii is large ($r_A/r_B > 1.46$). The A-site ($16d$) is eight-coordinated, while the B-site ($16c$) is six-coordinated, and the two cations alternate along the <110> direction. There are three distinct tetrahedrally coordinated anion sites: the $48f$ site that is coordinated with two A and two B cations, the $8b$ site that is coordinated with four A cations, and the vacant $8a$ site that is coordinated with four B cations. The x-position of the $48f$ site determines the shape of the A and B coordination polyhedra—an x-coordinate of 0.3125 indicates a perfect octahedral coordination for B, an x-position of 0.3750 indicates a perfect cubic coordination for A, and an intermediate value indicates some partial distortion of both polyhedra. These site labels are based on the origin being at the B-site.$^{38,29}$

The disordered pyrochlore structure, also known as defect-fluorite ($Fm-3m$), has one cation site and one anion site that is 7/8 occupied for pyrochlore compounds—the anion vacancy position is random. The defect-fluorite structure forms when the cationic radius ratio is small ($r_A/r_B < 1.46$). The cation site is coordinated by eight anions, which are coordinated by four cations. The single cation site means that the lattice parameter of defect-fluorite is half that of pyrochlore, such that the pyrochlore structure is an ordered 2×2×2 superstructure of the disordered defect fluorite, which is evidenced by pyrochlore superstructure peaks in X-ray diffraction. Furthermore, the anion sub-lattice of the defect-fluorite structure is equivalent to the pyrochlore anion sub-lattice with a $48f$ oxygen x-coordinate of 0.3750.$^{28,29}$

Subjecting pyrochlore to high pressure induces point defects—anti-site defects, where A and B cations switch sites, are the dominant type of cation defect, while Frenkel pairs are the dominant type of anion defect.$^{30–32}$ Although these defects play a critical role in the diverse applications of the pyrochlore structure-type,$^{14,33}$ the influence of intrinsic defect concentration on the response of pyrochlore to extreme environments has received little attention.$^{34,35}$

Here, we investigate the effect of atomic structure, concentration of cation anti-site and anion Frenkel defects, and internal strain on the high-pressure structural response of Dy$_2$Ti$_2$O$_7$ and Dy$_2$Zr$_2$O$_7$. The amount of strain and defect concentrations were controlled by mechanical milling followed by annealing at various temperatures. The ordered pyrochlore, Dy$_2$Ti$_2$O$_7$, with different initial defect concentrations, is compared with the inherently disordered pyrochlore, Dy$_2$Zr$_2$O$_7$, which has the defect-fluorite structure. Atomic order in the samples at ambient conditions was characterized using X-ray pair distribution function (PDF) analysis, Raman spectroscopy, and X-ray diffraction (XRD). Raman spectroscopy and XRD were again used to probe the material in situ at high pressure. Results show that the increased intrinsic strain and defect concentrations can lower the onset pressure of the phase transformation in ordered pyrochlore, and lower the completion pressure of the phase transformation in disordered pyrochlore.

### Results

#### Sample synthesis.

Samples were annealed at high temperature following ball milling—an overview of all samples, along with shorthand notation for sample names to be used herein, is shown in Table 1. Annealing of anion defects occurs at a critical temperature of ~750 °C for titanate pyrochlore$^{38}$ and ~1150 °C for zirconate pyrochlore$^{35}$. Cations are increasingly ordered as the annealing temperature is increased$^{36}$. For the ordered pyrochlore, Dy$_2$Ti$_2$O$_7$, unannealed samples had small amounts of both cation and anion order, while samples annealed at 800 °C had increased cation order and large amounts of anion order. Samples annealed at 1200 °C had large amounts of both cation and anion order. Cation anti-site defect concentrations for DT12, DT8, and DT0 samples were 0.03(2), 0.15(4), and 0.24(5), respectively, as quantified by Rietveld refinement of XRD data. Even with these caveats, the qualitative trend of continuously lower anti-site defect concentrations at higher annealing temperatures is consistent with thermally-induced defect recovery. We note that the defect-fluorite Dy$_2$Zr$_2$O$_7$ is inherently disordered due to its low radius ratio, but annealing temperatures of 1200 °C and 1500 °C were selected to be consistent with the behavior of ordered zirconate pyrochlore$^{35}$.

### Table 1.

Sample descriptions and results summary. Sample name, to be used as shorthand, indicates the composition of the sample as well as its annealing temperature. Summary of experimental results also provided.

| Sample name | Composition | Annealing temperature [°C] | Onset of transformation [GPa] | Completion of transformation [GPa] | Bulk modulus w/B′ = 8 [GPa] |
|-------------|-------------|---------------------------|-------------------------------|-----------------------------------|------------------------------|
| DT12        | Dy$_2$Ti$_2$O$_7$ | 1200                      | 34.2 (2.7)                    | not reached                       | 259 (5)                     |
| DT8         | Dy$_2$Ti$_2$O$_7$ | 800                       | 20.6 (1.8)                    | not reached                       | 231 (5)                     |
| DT0         | Dy$_2$Ti$_2$O$_7$ | N/A                       | ambiguous                     | not reached                       | 178 (5)                     |
| DZ15        | Dy$_2$Zr$_2$O$_7$ | 1500                      | 15.3 (1.3)                    | 37.4 (1.2)                        | 282 (15)                    |
| DZ12        | Dy$_2$Zr$_2$O$_7$ | 1200                      | 15.2 (2.4)                    | not reached                       | 282 (15)                    |
| DZ0         | Dy$_2$Zr$_2$O$_7$ | N/A                       | 17.1 (1.2)                    | 29.9 (2.0)                        | 282 (15)                    |

The ordered pyrochlore samples, along with shorthand notation for sample names to be used herein, is shown in Table 1. Annealing of anion defects occurs at a critical temperature of ~750 °C for titanate pyrochlore$^{38}$ and ~1150 °C for zirconate pyrochlore$^{35}$. Cations are increasingly ordered as the annealing temperature is increased$^{36}$. For the ordered pyrochlore, Dy$_2$Ti$_2$O$_7$, unannealed samples had small amounts of both cation and anion order, while samples annealed at 800 °C had increased cation order and large amounts of anion order. Samples annealed at 1200 °C had large amounts of both cation and anion order. Cation anti-site defect concentrations for DT12, DT8, and DT0 samples were 0.03(2), 0.15(4), and 0.24(5), respectively, as quantified by Rietveld refinement of XRD data. Even with these caveats, the qualitative trend of continuously lower anti-site defect concentrations at higher annealing temperatures is consistent with thermally-induced defect recovery. We note that the defect-fluorite Dy$_2$Zr$_2$O$_7$ is inherently disordered due to its low radius ratio, but annealing temperatures of 1200 °C and 1500 °C were selected to be consistent with the behavior of ordered zirconate pyrochlore$^{35}$. 
X-ray pair distribution function. X-ray PDF analysis (Fig. 1) shows the effects of annealing on short-to-medium range order. Annealing of defects following mechanical milling causes ~2.9% unit cell contraction in Dy$_2$Ti$_2$O$_7$, as can be observed by the systematic increase in bond length in DT0 as compared with DT8 and DT12 (Fig. 1a). This behavior is the opposite of that observed in Dy$_2$Zr$_2$O$_7$, where annealing of defects leads to ~2.6% unit cell expansion (Fig. 1b). Lines used to mark bond distances in Fig. 1 are based on the peak centers of the samples annealed at the highest temperature. A breakdown in medium-range order is observed in DT0, with peaks at a distance past one unit cell showing substantial broadening. While this broadening is observed at a similar length-scale in DZ0, it is not as significant.

X-ray diffraction. All samples undergo a high-pressure phase transformation to orthorhombic cotunnite (Pnma). Computational studies have shown that the cotunnite phase is a lower enthalpy structure than defect-fluorite or the compositionally equivalent amorphous phase for a variety of titanate and zirconate pyrochlore compositions at high pressure\cite{37-40}. Experimentally, many single-cation fluorite-structured oxides have been shown to transform to cotunnite at high pressure\cite{41,42}. However, the large amounts of disorder and strain inherent to the high-pressure cotunnite structure of the two-cation pyrochlore makes it difficult to definitively identify through XRD\cite{24,43}. For consistency between datasets, onset of the phase transformation is defined by an increase in scattering intensity between the (222) and (004) pyrochlore structure diffraction maxima (equivalent to (111) and (002) in the defect-fluorite structure) because this is the location of the most intense cotunnite peaks\cite{24,43}. This is quantified in Supplementary Fig. S3, which shows the increase in X-ray scattering from cotunnite as a function of pressure.

Selected XRD patterns from Dy$_2$Ti$_2$O$_7$ at various pressures are shown in Fig. 2, with the complete dataset provided in Supplementary Fig. S1. DT8 and DT0 show evidence of increased strain at low pressures as compared with DT12—as indicated by the broad, diffuse background\cite{36}—with DT0 showing more strain than DT8. All compounds experience a pressure-induced phase transformation. The onset of the phase transformation occurs at 34.2 GPa for DT12 and 20.6 GPa for DT8. An accurate transition pressure could not be identified in DT0 due to the large amount of strain even at low pressures. The increased scattering intensity between the (222) and (004) pyrochlore structure diffraction maxima at low pressure for DT8 and DT0 has been shown to originate from microstrain rather than an amorphous phase coexisting with pyrochlore\cite{36}. The transformations are not complete for all Dy$_2$Ti$_2$O$_7$ samples at the highest pressures studied.

Selected XRD patterns from Dy$_2$Zr$_2$O$_7$ at various pressures are shown in Fig. 3, with the complete dataset provided in Supplementary Fig. S2. DZ0 shows evidence of increased strain at low pressured as compared with
DZ15 and DZ12—as indicated by broader peak width. However, the amount of strain in all Dy₂Zr₂O₇ samples is less than what is seen in DT8 and DT0, as indicated by simple peak broadening as opposed to a broad, diffuse background. Similar to Dy₂Ti₂O₇, all samples experienced a high-pressure phase transformation, likely to the cotunnite phase. The onset of the phase transformation is identified as 15.3, 15.2 and 17.1 GPa for DZ15, DZ12, and DZ0, respectively. Transformations are fully complete at 37.4 GPa for DZ15 and 29.9 GPa for DZ0. The transformation of DZ12 is not complete by 44.5 GPa, the highest pressure studied.

Pressure-volume curves for both Dy₂Ti₂O₇ and Dy₂Zr₂O₇ are plotted in Fig. 4a and 4b, respectively. Values of the plotted data are given in Supplementary Table S1. Data are plotted out to a maximum of ~15–20 GPa. This maximum pressure was chosen because plotting out to too high of a pressure can include effects from structural distortions due to the creation of the high-pressure cotunnite phase⁴⁴, as well as increased non-hydrostaticity of the silicone oil pressure-transmitting medium⁴⁵. Data are fit with a third-order Birch-Murnaghan equation of state using EoSFit7-GUI⁴⁶ to determine the bulk moduli (B₀) of the samples. The pressure-derivative of bulk modulus (B₁) is held constant at 8 for all samples so a direct comparison of B₀ could be conducted. The bulk modulus of Dy₂Ti₂O₇ is shown to increase with annealing temperature; B₀ values for DT12, DT8, and DT0 were found to be 259(5), 231(5), and 178(5) GPa, respectively. In contrast, the bulk modulus of Dy₂Zr₂O₇ was found to be within 282(15) for DZ15, DZ12, and DZ0. The large amount of scatter in the zirconate diffraction data makes

Figure 2. High-pressure X-ray diffraction of Dy₂Ti₂O₇. Representative high-pressure XRD patterns for Dy₂Ti₂O₇ annealed at various temperatures: (a) 1200 °C, (b) 800 °C, (c) unannealed. Miller indicies of the pyrochlore structure are shown in (a). A transformation from pyrochlore to cotunnite occurs at high pressure. Value on the right of each diffraction pattern is pressure in GPa. Black dots in (c) indicate the presence of excess Dy₂O₃ in DT0.

Figure 3. High-pressure X-ray diffraction of Dy₂Zr₂O₇. Representative high-pressure XRD patterns for Dy₂Zr₂O₇ annealed at various temperatures: (a) 1500 °C, (b) 1200 °C, (c) unannealed. Miller indicies of the defect-fluorite structure are shown in (a). A transformation from defect-fluorite to cotunnite occurs at high pressure. Value on the right of each diffraction pattern is pressure in GPa.
it difficult to conclusively evaluate the bulk modulus of the individual samples, but plotted together a consistency between samples is clearly observed.

A summary of results—pressure of phase transformation onset/completion and bulk modulus—is given in Table 1.

**Raman spectroscopy.** Raman spectra from Dy$_2$Ti$_2$O$_7$ at various pressures are shown in Fig. 5. Raman modes prescribed to the pyrochlore structure are identified according to their Mulliken symbols in Fig. 5a. The broad mode between 700 and 800 cm$^{-1}$ is not a fundamental Raman mode in pyrochlore-structured oxides, and is believed to be due to distortions to the BO$_6$ octahedra. This mode is extremely weak in DT12 and extremely strong in DT0. The mode has moderate intensity in DT8, indicating that, even after heating past the critical temperature for anion defect annealing, there is still some increased distortion to the TiO$_6$ octahedra. However, the amount of anion disorder in DT8 is much less than that of DT0.

A pressure derivative of these data, calculated using Heun’s method, are given in Fig. 6b. This provides a way to determine the pressure at which the intensity ratio begins to increase. The ratio for DT0 increases at a near constant rate, with a slight increase at the highest pressure measured. In contrast, the ratios of DT8 and DT12 are relatively constant in the low-pressure regime, followed by a rapid increase at higher pressures. DT8 experiences an initial increase at 35 GPa, with a more rapid increase beginning at 40 GPa. DT12 experiences an initial increase at 35 GPa, with a more rapid increase beginning at 44 GPa. Error in these values are approximately 2 GPa. Values of the data plotted in Fig. 6a and b are given in Supplementary Table S2.

Raman spectra of Dy$_2$Zr$_2$O$_7$ could not be collected at high pressure due to the extremely weak signal even at long collection times. This may be related to the difficulties observed in collecting Raman spectra on powders of Dy$_2$Hf$_2$O$_7$, which is similar to Dy$_2$Zr$_2$O$_7$ in its physical properties.
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Discussion
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Figure 5. High-pressure Raman spectroscopy of Dy₂Ti₂O₇. Representative high-pressure Raman spectra for Dy₂Ti₂O₇ annealed at various temperatures: (a) 1200 °C, (b) 800 °C, (c) unannealed. Mulliken symbols of the Raman modes given in (a). Value on the right of each spectrum is pressure in GPa.

Figure 6. Pressure-induced anion disordering in Dy₂Ti₂O₇. (a) Ratio of intensity between the Raman mode of the distorted TiO₆ octahedra (I₂) and the main F₂g Raman mode of the ordered pyrochlore (I₁). This serves as a qualitative indicator of the progression of anion disorder as a function of pressure. Inset identifies the two modes in a representative high-pressure Raman spectrum. (b) Pressure derivatives of the intensity ratio data plotted in (a). This serves to better define the change in intensity ratio as a function of pressure. Inset focuses on the region of interest where the ratios begin to rapidly increase. Legends indicate the samples.
radius ratio of Dy_2Ti_2O_7 as compared with Dy_2Zr_2O_7 of interconnected BO_6 octahedra. Distortions to these polyhedra work to decrease the material's structural resist-

ance to compression. Since this polyhedron acts as the framework of the pyrochlore structure 52, decreased cation anti-site defects cannot be created since its structure is inherently disordered. Thus, oxygen atoms moving into interstitial sites (anti-Frenkel pairs) is the dominant defect type. Oxygen in their ideal sites act as a bridge between nearest-neighbor cations; that is, the two cations are bonded to the same oxygen. The movement of this oxygen to an interstitial site allows the cation-anti-site distance to contract, and annealing of the anti-Frenkel pair causes the cation-anti-site distance to expand back to its ideal value. The peak broadening and loss of medium-range order in DZ0 is less than that observed in DT0, consistent with the inability to further increase the anti-site defect concent-

ration in defect-fluorite Dy_2Zr_2O_7.

At moderate pressure — below the onset of the high-pressure phase transformation — material behavior is again seen to be dictated by its defects. Pressure-volume curves (Fig. 4) show that annealing temperature affects compressibility of Dy_2Ti_2O_7, but not Dy_2Zr_2O_7. This indicates that bulk modulus can be controlled by varying cation order — the trend of increasing bulk modulus with annealing temperature in Dy_2Ti_2O_7 shows that cation ordering increases bulk modulus. This is again consistent with the description of the pyrochlore structure as a framework of interconnected BO_6 octahedra. Distortions to these polyhedra work to decrease the material's structural resistance to compression.

All samples transform to the cotunnite structure at high pressure. The commonly accepted mechanism for the pressure-induced pyrochlore-to-cotunnite phase transformation requires initial disordering of the anion sub-lattice before the transformation can proceed 55, 53, 54. This anion disordering is tied to a decrease in the 48f oxygen x-position, meaning that anion disorder can be thought of as the more octahedral coordination of the B cation in pyrochlore transitioning to the more cubic coordination environment typical of defect-fluorite. If the B-site is in fully cubic coordination, then the two cation sites are functionally equivalent in terms of their anion coordination environments, so the A and B cations no longer have a site preference. This facilitates the transform-

ation to cotunnite, a phase with no cation site preferences 24, 41. Consistent with this mechanism is that transition pressure increases with cationic radius ratio 55 because a larger radius ratio increases the formation energy of both anion Frenkel pairs and cation anti-site defects 30–32.

The data here are consistent with this mechanism for the transition. For instance, the Raman spectra of DT12 (Fig. 5a) shows that the anion sub-lattice is fully-disordered by 55.1 GPa, while there is still a large phase fraction of pyrochlore, as evidenced by the XRD pattern (Fig. 2a) at 53.6 GPa. And the onset of the high-pressure cotun-

nite phase in DT12 (34.2 GPa) corresponds well with the onset of anion disorder (35 GPa). Also, the transition pressure of DT12 is much higher than the transition pressure of DZ15, which is expected due to the larger cationic radius ratio of Dy_2Ti_2O_7 as compared with Dy_2Zr_2O_7 23. However, this accepted transformation mechanism does not explain why DT12 has a higher transition pressure than DT8, or why DT8 begins to transform (20.6 GPa) before its anion sub-lattice begins to disorder (30 GPa). This can again be explained by examining the intrinsic defects in the sample at ambient conditions, and how these defects behave as pressure is increased.

In Dy_2Ti_2O_7, the transition pressure of DT12 (34.2 GPa) is significantly higher than the transition pressure of DT8 (20.6 GPa); this nearly 50% decrease in transition pressure is accompanied by only a ~10% reduction in bulk modulus, showing that the energetics of the phase transformation can be improved without sacrificing significant mechanical integrity. The decrease in transition pressure is ascribed to increased disorder in DT8 relative to DT12, though this raises the question of whether it is the increased cation or anion disorder that lowers the transition pressure. The markedly different behavior of anion disordering in DT0 as compared with DT8 and DT12 in Fig. 6a suggests that DT8 and DT12 still have similar anion sub-lattice behavior despite the greater amount of anion disorder in DT8 at ambient conditions. This is consistent with the fact that anion defects are mainly annealed at a critical temperature, while cation defects are constantly annealed as temperature increases 38. Thus, it is likely that increased cation disorder leading to strain lowers the transition pressure. In a well-ordered pyrochlore with little initial strain, disordering of anions is necessary in order to allow the phase transformation to occur. However, ample initial strain may sufficiently lower the enthalpy barrier of the phase transformation by increasing the internal energy of the pyrochlore phase such that anion disordering is no longer required 39. In effect, controlling the defect concentration in pyrochlore at ambient conditions allowed for the decoupling of the defects and cation sublattices at high pressure, in addition to the decreased transition pressure.

In contrast to Dy_2Ti_2O_7, the transition pressure of Dy_2Zr_2O_7 is within error for all three samples — DZ15, DZ12, and DZ0. This consistency is due to the fact that the cation and anion sub-lattices of the defect-fluorite structure are inherently disordered under ambient conditions. However, increased strain is shown to improve the kinetics of the phase transformation, with the transition in DZ0 completed at a pressure 20% less than that of DZ15 (29.9 vs. 37.4 GPa). The sluggishness of the transformation in DZ12—incomplete by 44.5 GPa—relative to DZ15 is likely due to the much smaller grain size of DZ12 34. Interestingly, this sluggishness does not extend to DZ0, which has an even smaller grain size than DZ12 35, but completes its transformation at the lowest pressure. Peak broadening in Fig. 3 shows significantly higher amounts of strain on the cation sub-lattice in DZ0 as compared with DZ12 or DZ15. Thus, increased strain promotes the transition to the high-pressure phase to the point it overcomes the effect of the smaller grain size. This increase in kinetics is not accompanied by any reduction in bulk modulus, illustrating the preservation of the material's mechanical integrity.
This mechanism of strain-enhanced phase transformation kinetics is consistent with swift heavy ion irradiation experiments where ZrO2 was irradiated in situ at high pressure46. ZrO2 undergoes a monoclinic-to-tetragonal phase transformation under irradiation, and a greater amount of tetragonal material was produced in samples irradiated at high pressure as compared with samples irradiated at ambient pressure. Furthermore, the amount of transformed material increased as pressure increased, substantiating the hypothesis that increased strain raises the enthalpy of the initial phase57, thus lowering the transition pressure. Both the monoclinic-to-tetragonal transformation in ZrO2 and the pyrochlore-to-cotunnite transformation in Dy2Ti2O7 are displacive58,59, so there is a physical basis for the expectation that internal strain would help to drive these transformations.

We have demonstrated that the concentrations of defects in pyrochlore under ambient conditions—and, thus, the material’s intrinsic strain—influences its response to high pressure, an applied source of extrinsic strain. Increases in intrinsic strain are shown to lower the onset pressure of the phase transformation in the ordered pyrochlore Dy2Ti2O7, and lower the completion pressure of the phase transformation in the disordered pyrochlore Dy2Zr2O7. These changes in the material’s phase behavior are not associated with significant changes in mechanical integrity, as described by the bulk modulus of the material.

Methods
Sample synthesis. Dy2B2O7 (B = Ti, Zr) powders were prepared through solid-state synthesis46. Dy2O3 was mixed with BO2 in a 1:2 ratio and ball milled for 19 hours to create stoichiometric Dy2B2O7. Milled powders were then annealed in air for 12 hours at either 1200 °C or 800 °C for Dy2Ti2O7 and either 1500 °C or 1200 °C for Dy2Zr2O7. Rietveld refinement on the integrated diffraction patterns 64. Representative Rietveld refinements for all samples are provided in Supplementary Fig. S4. Error in unit cell volume was quantified by fitting individual diffraction peaks in Fityk and taking the standard deviation of the volumes garnered from these peaks.

High-pressure loading. Samples were compressed to high pressure (~40–50 GPa) using a symmetric DAC with 300 μm diameter diamond culets. Ruby fluorescence was used to monitor pressure46. Error in the ruby measurement is ~1 GPa above 40 GPa, but is otherwise less than 0.5 GPa. Stainless steel gaskets were pre-indented to 25 μm, and a 120 μm diameter hole was drilled to serve as a sample chamber. Silicone oil was used as the pressure-transmitting medium45.

X-ray pair distribution function. X-ray PDF data were collected at beamline 11 ID-B of the Advanced Photon Source (APS), Argonne National Laboratory (ANL). X-ray energy was 90.50 keV (λ = 0.1370 Å). Polycrystalline powder samples were packed into polyimide capillaries (outer diameter of 0.0435” and length 514.5 nm laser wavelength and 10 mW laser power. Data were summed over ten accumulations, each of which contains X-ray pair distribution function.

X-ray diffraction. Angular dispersive XRD data were collected at beamlines 16 BM-D of the APS, ANL, and 12.2.2 of the Advanced Light Source (ALS), Lawrence Berkeley National Laboratory (LBNL). X-ray energies used were 25 (λ = 0.4959 Å), 29.2 (λ = 0.4246 Å), and 40 keV (λ = 0.3100 Å). A CeO2 standard was used as a calibrant. Collection time was 30 or 60 s depending on signal intensity. A Mar345 image plate detector was used to record diffraction data. Integration of raw diffraction data was performed using Dioptas63. Maud was used to perform Rietveld refinement on the integrated diffraction patterns64. Representative Rietveld refinements for all samples are provided in Supplementary Fig. S4. Error in unit cell volume was quantified by fitting individual diffraction peaks in Fityk and taking the standard deviation of the volumes garnered from these peaks.

Raman spectroscopy. Raman spectra were collected using a Renishaw RM1000 Raman microscope with 514.5 nm laser wavelength and 10 mW laser power. Data were summed over ten accumulations, each of which were 10 s in duration. Background subtraction was performed on the raw data before normalization. This background was attributed to scattering from the diamonds since it was largely absent from spectra recorded at ambient conditions.

Heun’s method, used to calculate the pressure-derivative of the intensity ratio (Fig. 6b), is defined as:

$$\frac{dIR}{dP} = \frac{1}{2} \left( \frac{IR_{i+1} - IR_i}{P_{i+1} - P_i} + \frac{IR_i - IR_{i-1}}{P_i - P_{i-1}} \right)$$

where IR is intensity ratio, P is pressure, i is the index of the data point, and dIR/dP is the change in intensity ratio with respect to pressure. This equation was modified to calculate dIR/dP at the endpoints, where either i + 1 or i − 1 does not exist, by only calculating the slope in one direction.

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Author Contributions

D.R.R., R.C.E., and W.L.M. conceived of the study. A.F.F. synthesized the samples. C.P. performed the experimental set-up and instrument calibration for the synchrotron X-ray diffraction. D.R.R., K.M.T., and S.P. carried out the experiments. D.R.R. processed and interpreted the data. D.R.R., R.C.E., and W.L.M. prepared the manuscript. All authors discussed the results and contributed to the manuscript.

Additional Information

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