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The birth of a galaxy – III. Propelling reionization with the faintest galaxies

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ABSTRACT

Starlight from galaxies plays a pivotal role throughout the process of cosmic reionization. We present the statistics of dwarf galaxy properties at z > 7 in haloes with masses up to 10^9 M☉, using a cosmological radiation hydrodynamics simulation that follows their buildup starting with their Population III progenitors. We find that metal-enriched star formation is not restricted to atomic cooling (T_{vir} ≥ 10^4 K) haloes, but can occur in haloes down to masses ~10^9 M☉, especially in neutral regions. Even though these smallest galaxies only host up to 10^7 M☉ of stars, they provide nearly 30 per cent of the ionizing photon budget. We find that the galaxy luminosity function flattens above M_{UV} = -12 with a number density that is unchanged at z ≲ 10. The fraction of ionizing radiation escaping into the intergalactic medium is inversely dependent on halo mass, decreasing from 50 to 5 per cent in the mass range log M/M☉ = 7.0–8.5. Using our galaxy statistics in a semi-analytic reionization model, we find a Thomson scattering optical depth consistent with the latest Planck results, while still being consistent with the UV emissivity constraints provided by Lyα forest observations at z = 4–6.

Key words: radiative transfer – methods: numerical – galaxies: dwarf – galaxies: formation – galaxies: high-redshift – dark ages, reionization, first stars.

1 INTRODUCTION

Cosmic reionization is an extended process as individual H II regions grow around ionizing sources that gradually coalesce, culminating in a fully ionized Universe by z ~ 6 (e.g. Gnedin & Ostriker 1997; Razoumov et al. 2002; Ciardi, Ferrara & White 2003; Sokasian et al. 2003; Furlanetto, Zaldarriaga & Hernquist 2004; Iliev et al. 2006; Robertson et al. 2010; Trac & Gnedin 2011; Zahn et al. 2011; So et al. 2014). However, there is still some tension between observational constraints on the timing and duration of reionization. First, the transmission fraction of z ~ 6 quasar light blueward of Lyα through the intergalactic medium (IGM) indicates that the Universe was mostly ionized by this epoch (e.g. Gunn & Peterson 1965; Fan et al. 2002, 2006; Willott et al. 2007; Mortlock et al. 2011). Secondly, observations of the cosmic microwave background (CMB) from the Wilkinson Microwave Anisotropy Probe (WMAP) and Planck have measured the optical depth to Thomson scattering τ_e = 0.089^{+0.012}_{-0.014}, which corresponds to the Universe being ~50 per cent ionized at z = 11.1 ± 1.1 (Planck Collaboration 2013). But the ionizing emissivity measured at z = 4–6 through Lyα forest observations cannot account for this measured τ_e, indicating that the end of reionization must be photon starved (Bolton & Haehnelt 2007) and that the emissivity must have been higher during reionization. Third, the duration of reionization has been constrained to occur within Δz < 7.9 by measuring the kinetic Sunyaev–Zel’dovich effect with the South Pole Telescope (Zahn et al. 2012). These observations suggest that reionization was an extended process, mainly occurring at 6 ≲ z ≲ 15.

What population of ionizing sources drives this global and extended transition? It is clear that quasars and the very brightest galaxies, both of which are too rare, do not significantly contribute to the overall ionizing photon budget of reionization (e.g. Shapiro 1986; Dijkstra et al. 2004; Willott et al. 2010; Grissom, Ballantyne & Wise 2014). Starlight from galaxies is thought to provide the vast majority of the ionizing photon budget from extrapolating the.
observed $z > 6$ galaxy luminosity function (LF) to low luminosities (e.g. Madau, Haardt & Rees 1999; Bouwens et al. 2012a; Fontanot, Cristiani & Vanzella 2012; Haardt & Madau 2012; Shull et al. 2012; Robertson et al. 2013). Additionally, massive, metal-free (Population III; Pop III) stars can contribute of the order of 10 per cent of the budget (Ricotti & Ostriker 2004a; Greif & Bromm 2006; Trac & Cen 2007; Wise & Abel 2008a; Ahn et al. 2012; Wise et al. 2012b; Johnson, Dalla & Khochfar 2013; Paardekooper, Khochfar & Dalla Vecchia 2013) because they are short lived (e.g. Tumlinson & Shull 2000; Schaerer 2002) and can be suppressed by chemical enrichment and $H_2$-dissociating radiative feedback (e.g. Haiman, Rees & Loeb 1997; Haiman, Abel & Rees 2000; Machacek, Bryan & Abel 2001; Wise & Abel 2008b). Finally, X-ray radiation from X-ray binaries and accreting massive black holes partially ionize the IGM and may contribute a small amount to the Thomson scattering optical depth (Ricotti & Ostriker 2004b; McQuinn 2012; Fragos et al. 2013; Power et al. 2013).

Deep galaxy surveys, such as the Hubble Ultra Deep Field (HUDF; Beckwith et al. 2006; Koekemoer et al. 2013) and CANDELS (Grogin et al. 2011; Koekemoer et al. 2011) can probe $z \gtrsim 6$ galaxies up to absolute UV magnitudes $M_{UV} < -18$ or equivalently a stellar mass of $M_\star \gtrsim 10^7 M_\odot$. Future deep surveys using the James Webb Space Telescope (JWST) and 30-m class ground-based telescopes will push this limit down to $M_{UV} \sim -15.5$. At these high redshifts, the faint-end LF slope is steepening with redshift and is around $-2$ at $z \sim 8$ (e.g. Bouwens et al. 2011; Bradley et al. 2012; Oesch et al. 2012). The least massive galaxies can be suppressed through supernovae (SNe) and/or radiative feedback, and this process should materialize as a flattening or turnover in the LF, but starting at which limiting magnitude?

Any change in the LF behaviour should be related to the star formation efficiency, i.e. $M_\star/M_{gas}$, which is also connected to the effectiveness of gas cooling and the halo mass in principle. For instance, starting at the lowest mass haloes, the primary coolants in the interstellar medium (ISM) are molecular hydrogen and metals (e.g. C, O, Si), whereas above a virial temperature $T_{vir} \sim 10^5$ K, they change to atomic hydrogen. Negative feedback in these small haloes is also a concern on whether they can sustain efficient star formation. Examples of such feedback include photoevaporation, $H_2$ dissociation, and gas blowout from HI regions and SN, which all depend on halo mass (e.g. Gnedin 2000; Wise & Cen 2009; Hopkins et al. 2013; Stinson et al. 2013). In the $H_2$-cooling haloes with $M \sim 10^7 M_\odot$, $H_2$ can be dissociated by a moderate Lyman–Werner (LW; 11.2–13.6 eV) background. But in more massive haloes with $M \sim 10^9 M_\odot$, cold gaseous reservoirs can form even in the presence of a strong LW radiation field (Wise & Abel 2007; Johnson, Greif & Bromm 2008; O’Shea & Norman 2008; Safranek-Shrader et al. 2012). Progressing up the mass scale, even atomic cooling haloes are prone to negative feedback; for example, haloes with masses $M \lesssim 2 \times 10^8 M_\odot$ can be photoevaporated by an external radiation field, gradually boiling away their star-forming gas reservoir (Efstathiou 1992; Thoul & Weinberg 1996; Dijkstra et al. 2004; Shapiro, Iliev & Raga 2004; Okamoto, Gao & Theuns 2008; Finlator, Davé & Özel 2011).

How does the LF limiting magnitude $M_{lim}$ affect reionization histories? Recently, a few groups (Finkelstein et al. 2012; Kuhlen & Faucher-Giguère 2012; Robertson et al. 2013) have explored this question among other variations in their reionization models. Kuhlen & Faucher-Giguère found a nearly linear dependence between $\tau_e$ and $M_{lim}$, increasing $\tau_e$ from $-0.06$ to $0.08$ when $M_{lim}$ increases from $-13$ to $-10$. Robertson et al. found little dependence on $M_{lim}$ above $-13$. Whereas Finkelstein et al. showed that the escape fraction must be greater than 30 and 50 percent to sustain reionization at redshifts 6 and 7, respectively, if only the observed CANDELS galaxies contribute to the emissivity. Additional constraints on reionization can be gained from the inferred ionizing flux in the Ly$\alpha$ forest at $z = 4–6$ (Bolton & Haehnelt 2007; Kuhlen & Faucher-Giguère 2012). Extrapolating the LF down to $M_{UV} = -13$ and assuming that the escape fraction $f_{esc}$ is independent of halo mass, Finkelstein et al. also found that $f_{esc} < 0.13$ is constrained by the measured ionizing photon emissivity in Ly$\alpha$ forest observations at $z = 6$. It is clear from these studies that a population of unobserved dwarf galaxies is primarily responsible for driving cosmic reionization.

To further refine reionization models, it is pertinent to determine the characteristic properties of these unobserved dwarf galaxies. In particular, the stellar fraction, $M_\star/M_{vir}$, and $f_{esc}$ of high-redshift galaxies are the largest sources of uncertainty in reionization models.2 Current reionization models favour scenarios that have a luminosity-weighted average escape fraction that increases with redshift to match the observed $\tau_e$ value while being photon starved at $z \sim 6$ (Alvarez, Finlator & Trenti 2012; Haardt & Madau 2012; Kuhlen & Faucher-Giguère 2012; Shull et al. 2012; Mitra, Ferrara & Choudhury 2013). For example, the model of Alvarez et al. considers a scenario where galaxies in haloes of mass $10^6 \lesssim M/M_\odot \lesssim 2 \times 10^8$ with $f_{esc} = 0.8$ dominate the ionizing emissivity at early times and are gradually photosuppressed (also see Sobacchi & Mesinger 2013). Then at $z \lesssim 6.5$, galaxies greater than $2 \times 10^7 M_\odot$ with lower average escape fractions become sufficiently abundant to produce the majority of ionizing photons, keeping the Universe ionized in a photon-starved scenario. Before moving forward, it should be stressed that the UV escape fraction is an intrinsic quantity for a given galaxy not an entire population. Galaxies with the same mass can have very different escape fractions, arising from, e.g. complex gaseous and stellar morphologies, dust content, and cosmological mass inflow. Furthermore, variable star formation rates (SFRs) and the associated radiative feedback in the ISM can result in an escape fraction that is highly time dependent.

The ionizing escape fraction is a notoriously difficult quantity to measure both in high-redshift galaxy observations and theoretical studies. Nevertheless, this topic has been a subject of great interest to constrain the reionization history of the Universe. On the observational side, it is nearly impossible to detect Lyman continuum (LyC) emission at $z > 4$ because the number density of Lyman limit systems rapidly increases with redshift (Inoue & Iwata 2008). However at $z \sim 3$ when the IGMC optical depth is around unity, detection of intrinsic LyC radiation becomes feasible. Deep narrow-band galaxy imaging and spectroscopy have uncovered LyC emission in 10–20 per cent of Lyman-break galaxies, which can be interpreted as the mean ionizing radiation escape fraction (Steidel, Pettini & Adelberger 2001; Shapley et al. 2006; Iwata et al. 2009; Nestor et al. 2011; Jones et al. 2013, but also see Vanzella et al. 2012).

Theoretical efforts have focused on the calculation of $f_{esc}$ for over a decade, using analytical and numerical techniques with varying model complexities. The galaxies studied in these cumulative works span over six orders of magnitude in halo mass and are considered out to $z = 15$. Models of the escape fraction found that $f_{esc} \lesssim 0.06$ for Milky Way like galaxies (Dove, Shull & Ferrara 2000), and, in

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2 Other properties that could affect the ionizing emissivity originating from such galaxies are the gas fraction, initial mass function (IMF), gaseous and stellar morphology, and the strength and duration of star formation events.
2 METHODS

We further analyse the ‘RP’ simulation originally presented in Wise et al. (2012a, hereafter W12), which focused on the role of radiation pressure during dwarf galaxy formation. In this paper, we will focus on the LF, escape fraction of UV radiation, and the role of these first galaxies during reionization. A detailed description of the radiative cooling, star formation, and stellar feedback models is given in W12, thus we only briefly describe the input physics and methods in this section.

2.1 Simulation setup

This simulation was run with the adaptive mesh refinement (AMR) code enzo v2.0.1 (The Enzo Collaboration et al. 2013). It uses an N-body adaptive particle-mesh solver (Efstathiou et al. 1985; Couchman 1991; Bryan & Norman 1997) to follow the dark matter (DM) dynamics. It solves the hydrodynamics equations using the second-order accurate piecewise parabolic method (Woodward & Colella 1984; Bryan et al. 1995), while an Harten-Lax-van Leer-Contact (HLLC) Riemann solver ensures accurate shock capturing with minimal viscosity. We use the nine species \( \ {\mathrm{H}_1, \ H_2, \ H_3, \ H_4, \ H_5, \ e^-, \ e^+, \ \text{He}^2, \ \text{He}^3} \) non-equilibrium chemistry model in enzo (Abel et al. 1997; Anninos et al. 1997) and the \( \text{He}^+ \) cooling rates from Glover & Abel (2008). In addition to the primordial radiative cooling, we include metal and molecular line cooling, using cooling rates that are calculated with cloudy (Smith, Sigurdsson & Abel 2008).

We initialize a simulation of 1 comoving Mpc on a side at \( z = 130 \) with a base resolution of 256, using gramic (Bertschinger 2001) with the 7-year WMAP+SZ+LENSS best fit (Komatsu et al. 2011): \( \Omega_M = 0.266, \Omega_\Lambda = 0.734, \Omega_b = 0.0449, h = 0.71, \sigma_8 = 0.81, \) and \( n = 0.963 \) with the variables having their usual definitions. The DM mass resolution is 1840 M\( \odot \), and the maximum spatial resolution is 1.0 comoving pc or 12 levels of AMR refine. We refine the grid on baryon overdensities of \( 3 \times 2^{-0.2l} \), where \( l \) is the AMR level. We also refine on a DM overdensity of three and always resolve the local Jeans length by at least four cells, avoiding artificial fragmentation during gaseous collapses (Truelove et al. 1997). If any of these criteria are met in a single cell, it is flagged for further spatial refinement. We stop the simulation at \( z = 7.3 \) when the simulation box is 70 per cent ionized by volume, and the ray tracing from ~1000 point sources becomes computationally expensive in the optically thin regime. We analyse the simulation from outputs that are written 12.5 Myr apart until \( z = 8 \) and then every 1 Myr until the final redshift.

2.2 Star formation and feedback

We use distinct star formation and feedback models for Pop II and III with the latter forming when the gas metallicity of the star-forming gas is below \( 10^{-4} Z_\odot \). The star formation criteria are similar to the original Cen & Ostriker (1992) model but with a critical \( \text{H}_2 \) fraction for Pop III star formation, and for Pop II stars, the model has been modified to allow for star-forming clouds that are Jeans resolved. We model the formation, main sequence, and stellar end-points of these populations with the following characteristics.

(i) Pop II. Each star particle represents a stellar cluster with a minimum mass \( M_{\text{min}} = 1000 \, M_\odot \) and a Salpeter IMF. The initial mass function is modified to allow for star-forming clouds that are Jeans resolved.

(ii) Pop III. Each star particle represents a single massive star with a minimum mass of \( 10^3 \, M_\odot \). The stars are born with a Salpeter IMF and explode as supernovae after a fixed time.

(iii) Feedback. Star formation is feedbacked as a combination of ionizing and UV radiation, which escape from the star particles to the surrounding gas. The ionizing radiation is calculated with cloudy, and the UV radiation is accounted for in the gas cooling rates.
accretion event converts 7 per cent of the cold \((T < 1000\ \text{K})\) gas within a sphere with a dynamical time of 3 Myr \((\rho \approx 1000\ \mu\text{cm}^{-3})\) into a star particle (see W12). If the initial star particle is less than 1000\(M_\odot\), then the star particle continues to accrete until it reaches this threshold. In the case where it does not reach \(M_{\text{max}}\) within a dynamical time of 3 Myr, the accretion halts at this point, and the star particle begins to radiate. Star particles only emit radiation after this accretion phase is completed. They emit 6000 hydrogen ionizing photons per stellar baryon over a lifetime of 20 Myr. We consider a monochromatic spectrum with an energy of 21.6 eV (Schaerer 2003). After living for 4 Myr, they generate \(6.8 \times 10^{16}\ \text{erg s}^{-1}\ \text{M}_\odot^{-1}\) in SNe energy that are injected into resolved spheres of radius 10 pc.

(ii) Pop III. Each star particle represents a single star whose mass is randomly drawn from a power-law IMF that exponentially decays below a characteristic mass \(M_{\text{char}} = 100\ \text{M}_\odot\),

\[
f(\log M) dM = M^{-1.3} \exp \left[- \left( \frac{M_{\text{char}}}{M} \right)^{1.6} \right] dM.
\]

The mass-dependent hydrogen ionizing and LW photon luminosities and lifetimes are taken from Schaerer (2002). We consider a monochromatic spectrum with an energy of 29.6 eV, appropriate for the near-constant 10\(^5\) K surface temperatures of Pop III stars. The SN explosion energies and metal ejecta masses from Nomoto et al. (2006) and Heger et al. (2003) are used for Type II \((20–40\ \text{M}_\odot)\) and pair instability SNe \((140–260\ \text{M}_\odot)\), respectively. We do not consider any SN feedback from Pop III stars in the mass range 40–140\(\text{M}_\odot\) because they most likely collapse into a black hole without an explosion (Heger et al. 2003).

The hydrogen ionizing radiation emitted during main sequence are propagated with adaptive ray tracing (Abel & Wandelt 2002; Wise & Abel 2011) that is based on the realpks framework (Górski et al. 2005). The radiation field is evolved at every hydrodynamics time step of the finest AMR level that is of the order of 10 kyr. The photoheating that occurs on these time steps couples the radiation effects to the hydrodynamics. In addition, this simulation considers the momentum transfer from ionizing radiation to the absorbing gas, i.e. radiation pressure. We model the LW radiation with a time-dependent optically thin soft UV background and add inverse square profiles, centred on all Pop II and III star particles, to estimate the total LW radiation at all points. Using this physics set, we have shown in W12 that the galaxies produced in this simulation match the luminosity–metallicity relation for local dwarf galaxies and does not suffer from the well-known galaxy overcooling problem seen in many previous galaxy formation simulations.

3 SIMULATION RESULTS

The previous two papers in this series studied the individual properties of selected galaxies.\(^4\) In this work, we study the global statistics of galaxies, in particular, their stellar masses, SFRs, gas fractions, LF, the fraction of escaping UV radiation, and their contribution to reionization. The stellar radiation from these galaxies reionize 70 per cent of the simulation volume by \(z = 7.3\), and the ionization history is shown in Fig. 1. It should be noted that this history is not cosmologically representative as a simulation box of \(\gtrsim 100\ \text{Mpc} h^{-1}\) is required (e.g. Iliev et al. 2006, 2013) for such a study. However,

\(^4\) We define a galaxy as any metal-enriched stellar system that is gravitationally bound and exists in a dark matter halo (Willman & Strader 2012).
Pop III stars. The largest halo has which has been enriched by a nearby SN and did not form any in Table 1. Because the galaxy formation suppression shown in Fig. 1 for a plot of ionization history. Star formation in the non-atomic cooling haloes \((M_{\text{vir}} < 10^8 M_\odot)\) occurs at high redshift, only to be suppressed by external radiative feedback.

the haloes must then accrete from a pre-heated IGM. The filtering mass,
\[
M_{\text{filter}}^\text{a/3}(a) = \frac{3}{a} \int_0^a da' M_{\text{filter}}^{\text{a/3}}(a') \left( 1 - \frac{a'}{a} \right),
\]
is an analytical measure of the minimum mass of a Jeans-unstable halo in such a situation. Here \(a\) and \(M_1\) are the scalefactor and time-dependent Jeans mass of the accreted gas (Gnedin & Hui 1998; Gnedin 2000). The Jeans mass in the ionized regions is approximately \(4 \times 10^7 M_\odot\) at \(z = 20\) and increases to \(10^8 M_\odot\) by \(z = 7\) for a gas at the mean baryon density and \(T = 10^4 K\). The filtering mass correspondingly increases from \(10^7 M_\odot\) at \(z = 15\) to \(10^8 M_\odot\) at \(z = 7\) (see Wise et al. 2012b). Similar but not as severe suppression occurs at \(M_{\text{vir}} = 10^8 M_\odot\) in which \(f_{\text{host}}\) is around 0.5 at \(z \gtrsim 12\) \((\sim 0.1)\) and decreases to \(\sim 0.15\) afterwards. These remaining 15 percent of galaxies are not actively forming stars, but they host stars that formed in their initial star formation event and have not accreted additional mass. Atomic cooling haloes with \(M_{\text{vir}} \gtrsim 10^8 M_\odot\) all host galaxies at \(z \gtrsim 8\). After this time, star formation in half of the \(M_{\text{vir}} = 10^8 M_\odot\) haloes is suppressed because the filtering mass is now \(\sim 10^7 M_\odot\).

Although mass accretion and star formation histories differ from halo to halo, the stellar and gaseous properties exhibit general trends with respect to halo mass with some interhalo variations. Fig. 4 shows the time-averaged stellar masses \(M_\star\), SFRs, star formation efficiencies \(f_\star = M_\star / M_{\text{gas}}\), gas fraction \(f_{\text{gas}} = M_{\text{gas}} / M_{\text{vir}}\), bolometric luminosity \(L_{\text{bol}}\), and AB magnitude \(M_{\text{UV}}\) at 1500Å of all of the galaxies as a function of halo mass. We calculate \(L_{\text{bol}}\) and \(M_{\text{UV}}\) using the stellar population synthesis model GALAXEV (Bruzual & Charlot 2003), using the star particle ages, masses, and metallicities as input into GALAXEV and assuming an instantaneous burst model for each Pop II star particle. We do not consider any nebular emission. The shaded regions in the figure show the PDF that is weighted by the time between outputs and is normalized in each column. The points show the average values and 1σ deviations in bins of 0.5 dex, which are also shown in Table 1.

3.2 Dwarf galaxy properties

At the redshift \(z = 7.3\) of our simulation, there are 32 haloes that host metal-enriched star formation. The smallest such halo has a virial mass \(M_{\text{vir}} = 7.6 \times 10^5 M_\odot\) and stellar mass \(M_\star = 840 M_\odot\), which has been enriched by a nearby SN and did not form any Pop III stars. The largest halo has \(M_{\text{vir}} = 6.8 \times 10^8 M_\odot\) and \(M_\star = 3.7 \times 10^8 M_\odot\). Here we define the halo as a sphere that contains an overdensity of \(18\pi^2\) relative to the critical density. There exists a wide range of stellar and gaseous mass fractions between these extremes. Because these low-mass haloes are heavily affected by stellar feedback, they cycle between quiescence and star-forming phases during their histories (e.g. Wise et al. 2012b; Hopkins et al. 2013). To capture the whole range of halo and galaxy properties from our small set of simulated dwarf galaxies, we present our results from all redshifts until the final redshift. During inhomogeneous reionization, we have found that MC halo properties are more dependent on environment (i.e. neutral or ionized) instead of halo mass because they must re-accrete gas to form stars after Pop III stellar feedback ejects the majority of their gas. Fig. 3 illustrates the evolution of galaxy occupation fraction \(f_{\text{host}}\), i.e. haloes that host metal-enriched stars, that is divided into five different mass bins with a width of 0.5 dex. The time-averaged values of \(f_{\text{host}}\) are shown in Table 1. Because the galaxy formation suppression shown in Fig. 3 is dependent on the particular reionization history of this simulation, the ionization fraction \(x\), not the exact redshifts in this small box simulation, should be used when applying these data.

At the low-mass range at early times, galaxies form in about one-third of the haloes with \(M_{\text{vir}} = 10^7 M_\odot\), and this fraction steeply decreases after \(z \sim 15\) \((x \sim 0.02)\) to 1 per cent within a halo sound-crossing time \(t_{\text{sc}} \sim 100\) Myr (Shapiro et al. 2004). These low-mass galaxies are some of the first to form in the simulation and ionize the surrounding IGM. The subsequent suppression occurs because

**Figure 2.** Fractional radiative cooling rates from atomic processes (red), fine-structure metal transitions (green), and \(H_2\) transitions (blue) as a function of time and halo mass, displayed as RGB colours and averaged over all haloes. The sum of each RGB channel in a cell is normalized to unity. The thick white line shows the halo mass corresponding to a virial temperature of \(10^4\) K. There is a clear transition from \(H_2\)-cooling to metal cooling at \(M_{\text{vir}} \gtrsim 10^7 M_\odot\) and to atomic cooling at \(T_{\text{vir}} = 10^4\) K. Haloes with \(T_{\text{vir}} < 10^4\) K can partially cool through recombination radiation in H \(\pi\) regions, depicted by the olive and purple shades for metal-enriched and metal-free haloes, respectively.

**Figure 3.** The fraction of haloes that host metal-enriched stars as a function of time in five different mass bins. The corresponding ionization fraction is shown on the upper axis. See Fig. 1 for a plot of ionization history. Star formation in the non-atomic cooling haloes \((M_{\text{vir}} < 10^8 M_\odot)\) occurs at high redshift, only to be suppressed by external radiative feedback.
The faintest galaxies during reionization

Table 1. General galaxy and host halo properties.

| log $M_{\text{vir}}$ ($M_\odot$) | log $M_*$ ($M_\odot$) | ($f_{\text{host}}$) | log $f_*$ | $f_{\text{gas}}$ | $M_{\text{UV}}$ | log $L_{\text{bol}}$ (L_\odot) | log $N_{\text{ion}}$ (ph s^{-1}) |
|-----------------|-----------------|-----------------|----------|----------|----------------|-----------------|-----------------|
| 6.5             | 3.41^{+0.10} -0.06 | 2.4 × 10^{-4}   | -1.88^{+0.35} -0.43 | 0.05^{+0.02} -0.03 | -5.61^{+0.73} -0.86 | 4.81^{+0.29} -0.31 | 49.2^{+0.1} -0.2 |
| 7.0             | 3.59^{+0.24} -0.33 | 0.052           | -2.25^{+0.11} -0.50 | 0.06^{+0.02} -0.03 | -6.09^{+1.35} -0.93 | 5.02^{+0.26} -0.29 | 49.5^{+0.2} -0.1 |
| 7.5             | 3.88^{+0.18} -0.29 | 0.28            | -2.48^{+0.27} -0.32 | 0.07^{+0.01} -0.02 | -7.17^{+1.30} -1.22 | 5.43^{+0.42} -0.50 | 49.6^{+0.3} -0.4 |
| 8.0             | 4.60^{+0.30} -0.12 | 0.90            | -2.25^{+0.15} -0.04 | 1.0^{+0.02} -0.02 | -9.59^{+0.87} -0.95 | 6.39^{+0.39} -0.39 | 49.9^{+0.3} -0.3 |
| 8.5             | 5.74^{+0.31} -0.37 | 1.0             | -1.80^{+0.23} -0.21 | 0.13^{+0.00} -0.00 | -13.72^{+0.82} -0.82 | 8.06^{+0.26} -0.26 | 51.6^{+0.1} -0.1 |

Notes: Statistics are shown for galaxies at all times in 0.5 dex bins in $M_{\text{vir}}$. Column (1): virial mass. Column (2): stellar mass. Column (3): time-averaged galaxy occupation fraction of haloes. See Fig. 3 for the time dependent of this fraction. Column (4): star formation efficiency, $M_*/M_{\text{gas}}$. Column (5): gas mass fraction. Column (6): UV magnitude at 1500 Å. Column (7): bolometric luminosity. Column (8): ionizing photon luminosity from young (<20 Myr) stars. Errors shown are 1σ deviations.

Figure 4. Clockwise from the upper left: stellar mass, SFR, gas mass fraction, bolometric stellar luminosity, absolute UV magnitude at 1500 Å from the stellar component, and star formation efficiency of all star-forming haloes at all redshifts. The pixels show the PDF that is weighted by the time between snapshots. The points and error bars show the mean values and standard deviations in 0.5 dex bins, respectively. The increase in SFRs and luminosities at $10^8 M_\odot$ are caused by higher gas fractions and more efficient radiative cooling through atomic hydrogen line transitions. Below this mass scale, star formation is induced primarily through metal fine-structure line and H2 cooling.

The stellar mass and SFRs in MC haloes exhibit less of a dependence on halo mass than atomic cooling haloes with $M_*$ increasing from $10^{10}$ to $10^{11} M_\odot$ over a halo mass range $log M_{\text{vir}} = [6.5, 7.5]$. In comparison, $M_*$ increases by almost two orders of magnitude over the next decade of halo mass. Correspondingly, similar behaviour is seen in their SFRs, absolute UV magnitudes, and bolometric luminosities. What causes this change in behaviour? We can gain some insight by exploring how $f_{\text{gas}}$ and $f_*$ vary with halo mass. We see that the average value of $f_*$ only varies by a factor of 3 around 0.01 over the entire mass range with a minimum at $M_{\text{vir}} = 10^5 M_\odot$. This concavity in $f_*$ is caused after the galaxy experiences its first Pop II star formation event, whose feedback suppresses any further star formation until the gas reservoir is replenished. During this suppression phase and after the outflows have ceased, the halo gas mass increases as the stellar mass remains constant, leading to a decrease in $f_*$ as shown in the plot. Furthermore, once the halo can cool through atomic line transitions, the star formation efficiency increases. On the other hand, the average value of $f_{\text{gas}}$ steadily increases from 0.05 at $M_{\text{vir}} = 10^6 M_\odot$ up to 0.13 in $10^8 M_\odot$ haloes. The larger scatter in low-mass haloes originates from their susceptibility to internal and external radiative and SN feedback. Varying degrees of feedback are caused by differing Pop III stellar masses that their progenitors hosted. At $M_{\text{vir}} > 10^7 M_\odot$, the gravitational potential well is deep enough so that the outflows only contain a small mass fraction. Thus, we conclude that both the increase in the star formation efficiency and gas mass fraction cause the greater SFRs as haloes transition from H2 and metal cooling to atomic line cooling.
3.3 Luminosity functions

We have shown that galaxies begin to form in haloes that rely on H$_2$ and metal cooling but not atomic line cooling. Recall that these haloes can have masses below the filtering mass. During this phase, star formation is less efficient than larger haloes with $T \gtrsim 10^4$ K. Afterward, they transition to more efficient star formation in atomic cooling haloes, which can be gradual or sudden if a galaxy experiences a major merger or not, respectively. These two different modes of galaxy formation should manifest in the galaxy LF at high $(M_{UV} \gtrsim -15)$ magnitudes.

Before constructing LFs from our data, we first check whether our small-scale (1 comoving Mpc$^3$) simulation is representative of the cosmic mean. Fig. 5 shows the simulated halo mass function against the analytical mass function of Warren et al. (2006) that is calibrated against a suite of $N$-body simulations. In our simulated volume, the halo mass function is consistent with analytical expectations at $M > 5 \times 10^5 M_{\odot}$, and below this mass scale, the simulated halo mass function is below the analytical fit because these small haloes are not well resolved, which does not affect the LF because galaxies do not form in such small haloes.

In order to understand the behaviour of the galaxy LF at $M_{UV} \gtrsim -15$, we calculate the simulated LF at several redshifts $z = \{7.3, 8, 9, 10, 12, 15\}$, which are shown in Fig. 6 in red squares. For comparison, we also plot the observed galaxy LFs and their fits from the HUDF galaxies at $z \leq 10$ (Bouwens et al. 2011; Oesch et al. 2013). It is clear that these dwarf galaxies do not follow the same power law found in $L^*$ galaxies at similar redshifts, but their LF is nearly flat at $M_{UV} \gtrsim -12$. The mean values and their standard deviations are displayed in Table 2. All of the galaxies with these magnitudes exist in MC haloes with $M_{\text{vir}} \lesssim 10^8 M_{\odot}$ (see Fig. 4). The comoving density of these haloes only varies by a factor of a few during the redshift range 7–15 (Mo & White 2002). Effects from radiative and SN feedback discussed in the previous section and the weakly varying halo number density can explain this flat.

### Table 2. Mean dwarf galaxy LF at $M_{UV} > -12$

| Redshift | $\phi$ (mag$^{-1}$Mpc$^{-3}$) |
|----------|-------------------------------|
| 7.3      | $2.2 \pm 1.4$                |
| 8        | $2.3 \pm 1.2$                |
| 9        | $2.5 \pm 1.2$                |
| 10       | $1.5 \pm 0.8$                |
| 12       | $1.2 \pm 0.6$                |
| 15       | $0.7 \pm 0.2$                |
and 8 HUDF LFs. As seen in Fig. 4, nearly all of the galaxies with haloes, and their number densities are consistent with the mass enough to host efficient star formation in atomic cooling.

Only at \( z \leq 8 \) in the simulation, a few galaxies with \( M \lesssim -12 \) are massive enough to host efficient star formation in atomic cooling haloes, and their number densities are consistent with the \( z = 7 \) and 8 HUDF LFs. As seen in Fig. 4, nearly all of the galaxies with \( M_{UV} \leq -12 \) are in the \( M_{vir} = 10^{13} \) mass bin, and the galaxies dimmer than this threshold are hosted by less massive haloes. This kink in the LF signifies the transition from \( \text{H}_2 \) and metal cooling to atomic cooling. The intersection between the LFs from the HUDF galaxies and our simulated galaxies is highly dependent on the slope \( \alpha \). In the \( z = 9 \) and 10 observed LF, the value for \( \alpha \) is fixed to \(-1.73 \) (Oesch et al. 2013), whereas at \( z = 7 \) and 8, there exists enough sub-\( L^* \) galaxies to fit \( \alpha = -2.01 \pm 0.21 \) and \(-1.91 \pm 0.32 \), respectively. Because we have found the LF to be flat and time independent at \( M_{UV} \gtrsim -12 \), the transition to a flat LF should only depend on the normalization \( \phi^* \) and slope \( \alpha \) of more luminous galaxies.

### 3.4 Escape fraction

The progression of cosmic reionization from stellar sources is inherently dependent on the ionizing photon luminosity, which primarily originate from massive stars, and how much of this radiation escapes into the IGM. The production rate of ionizing photons \( \dot{N}_{\text{phot}} \) of a stellar population can range from 4.1 to 1300 for a metal-poor (\( [Z/H] = -3.3 \)) population (Nagamine et al. 2009). Then a fraction \( f_{\text{esc}} \) of the emitted photons escape into the IGM. This quantity is the most uncertain of the four factors that enter into reionization calculations and has been the focus of several observational and numerical campaigns.

#### 3.4.1 Method

Radiative and SN feedback can create channels of diffuse ionized gas from the galaxy centre to the IGM, where photons can escape from the halo relatively unobscured. Because our simulation includes both of these effects, we can calculate the UV escape fraction in post-processing without any loss in accuracy. However, we do lose any variations that might occur between data outputs.

We define \( f_{\text{esc}} \) as the fraction of stellar photons that exit a sphere with radius \( r_{\text{vir}} \) located at the halo centre of mass. The UV escape fraction is directly related to the \( \text{H}_1 \) column density \( N_{\text{HI}} \) between each star and this sphere. We first divide the spherical surface into 768 \textsc{healpix} (level 3) equal-area pixels. Then for each star particle, we compute \( N_{\text{HI}} \), between the particle and the ith pixel, which is converted into a transmittance \( T_i \) in that particular line of sight,

\[
T_i = \exp(-\sigma_{\text{HI}} N_{\text{HI},i}),
\]

where we take the \( \text{H}_1 \) cross-section \( \sigma_{\text{HI}} = 1.78 \times 10^{-18} \) cm\(^2\) at 21.6 eV, which is the same energy as the radiation considered in the simulation (Verner et al. 1996). Because the sphere is divided into equal-area pixels, the escape fraction for a single star particle is the average transmittance \( T \) over all of the pixels, and \( f_{\text{esc}} \) for the entire halo is the luminosity-weighted average of \( T \),

\[
f_{\text{esc}} = \sum_{n} \frac{L_{\text{ion},n} T_n}{\sum_{n} L_{\text{ion},n}},
\]

where \( L_{\text{ion},n} \) is the ionizing luminosity in the halo.

#### 3.4.2 Global trends

Our main results for the escape fraction are shown in Fig. 7. We analyse the data similar to our approach with the average halo properties, where we calculate the PDF for all actively star-forming haloes at all times. Here we only include galaxies with young (<20 Myr) stars because massive OB stars emit almost all of the ionizing photons in a given stellar population. In addition, we use this same age criterion to determine which star particles emit ionizing radiation in the simulation. The red circles in this figure represent the mean quantity in 0.5 dex bins of \( M_{\text{vir}} \), and the blue squares denote the luminosity-weighted average of the quantities. These averages and their 1σ deviations are listed in Table 3.
The top panel of Fig. 7 shows the behaviour of \( f_{\text{esc}} \) with respect to halo mass. The lowest mass haloes with masses \( 10^6 \text{ to } 10^7 \text{ M}_\odot \) have \( f_{\text{esc}} \) around 50 per cent for both the mean and luminosity-weighted averages. This fraction then decreases with increasing halo mass. In the \( 10^{7.5} \text{ M}_\odot \) bin, \( f_{\text{esc}} \) is 30 per cent, shrinking to a mean and luminosity-averaged value of 10 and 25 per cent, respectively, for \( 10^9 \text{ M}_\odot \) haloes. The large scatter in the MC haloes is created by a wide spread in the gas fraction \( f_{\text{gas}} \) and star formation efficiency \( f_s \) (see Fig. 4), where radiation in a gas-poor halo propagates through a smaller neutral column, resulting in a higher escape fraction, and vice versa. Only 5 per cent of the ionizing radiation escape from the largest haloes (\( M_{\text{vir}} \geq 10^{12} \text{ M}_\odot \)) in the simulation.

The middle and bottom panels of Fig. 7 show the behaviour of the products \( f_{\text{esc}} f_s \) and \( f_{\text{esc}} f_s f_{\text{gas}} \). These products are essential ingredients in semi-analytic, and seminumerical reionization calculations and numerical simulations that do not resolve the multiphase ISM of such small galaxies. In Section 3.2, we showed that even the MC haloes can form stars at an appreciable rate with average values of \( f_s \) just under 0.01 for typical star-forming minihaloes. The decrease in \( f_{\text{esc}} \) dominates the downward trend in these products with respect to halo mass. The product \( f_{\text{esc}} f_s \) decreases from \(-2.8 \) to \(-3.6 \) (\(-2.3 \) to \(-3.0 \)) in the halo mass range \( 10^3 \text{ to } 10^7 \text{ M}_\odot \) for the mean (luminosity-averaged) values. Similarly, the product \( f_{\text{esc}} f_s f_{\text{gas}} \) decreases from \(-3.9 \) to \(-4.5 \) (\(-3.2 \) to \(-3.9 \)) for the mean (luminosity-averaged) values in the same mass range. This suggests that MC haloes may contribute significantly to the ionizing photon budget. To further demonstrate their contribution, Fig. 8 shows the normalized cumulative escaping ionizing photon emissivity as a function of halo mass at \( z = 12, 10, 8, 7.3 \) when the total ionizing emissivity of escaping photons is \((0.5, 0.9, 3.1, 7.3) \times 10^{50} \text{ s}^{-1} \text{ cMpc}^{-3} \) at \( z = (12, 10, 8, 7.3) \), respectively.

### Table 3. UV escape fraction.

| \( \log M_{\text{vir}} \) | \( f_{\text{esc}} \) | \( f_{\text{esc}} \) mean | \( f_{\text{esc}} \) mean | \( f_{\text{esc}} \) luminosity-weighted mean |
|----------------|-------|----------------|----------------|----------------|
| (1)            | (2)   | (3)           | (4)           | (5)           |
| 6.5            | 0.49+0.21 | -2.75±0.15 | -3.91±0.22 | -2.44±0.25 |
| 7.0            | 0.45+0.18 | -2.80±0.53 | -3.95±0.52 | -2.26±0.50 |
| 7.5            | 0.27+0.14 | -3.25±0.50 | -4.36±0.51 | -2.60±0.35 |
| 8.0            | 0.10+0.01 | -3.57±0.36 | -4.54±0.32 | -2.90±0.67 |
| 8.5            | 0.04+0.01 | -3.58±0.59 | -4.44±0.61 | -3.00±0.55 |

**Notes:** Statistics are shown for galaxies at all times in 0.5 dex bins in \( M_{\text{vir}} \). Column (1): virial mass in units of \( M_\odot \). Column (2): fraction of hydrogen ionizing radiation that escapes the virial radius. Column (3): product of the UV escape fraction and star formation efficiency. Column (4): product of column (3) and the gas mass fraction. Columns (5–7): same as columns (2–4) but ionizing luminosity-weighted means are shown. Errors shown are 1σ deviations.

### Figure 8. Normalized cumulative probability function of the ionizing emissivity of photons that escape into the IGM as a function of halo mass at redshifts 12 (dotted), 10 (dot-dashed), 8 (dashed), and 7.3 (solid). The shift to higher halo masses demonstrates that low-mass haloes provide a significant fraction of the ionizing photon emissivity at early times. The total ionizing photon emissivity is \((0.5, 0.9, 3.1, 7.3) \times 10^{50} \text{ s}^{-1} \text{ cMpc}^{-3} \) at \( z = (12, 10, 8, 7.3) \), respectively.

### Figure 9. Same as Fig. 7 but showing the UV escape fraction as a function of star formation efficiency \( f_s \) and sSFR.

In principle, the luminosity-weighted average is always higher than the mean value. This occurs because, at a fixed halo mass, galaxies with higher luminosities will ionize their ISM and create ionized channels out to the IGM more efficiently, boosting \( f_{\text{esc}} \) in such galaxies. To explore any correlation between the escape fraction and star formation, we plot the PDF of \( f_{\text{esc}} \) as a function of the star formation efficiency \( f_s \) and the specific star formation rate (sSFR = SFR/M_* in Fig. 9. The mean \( f_{\text{esc}} \) as a function of these quantities are also listed in Table 4. The escape fraction has a gradual upward trend in the range \( f_s = 10^{-4} \text{ to } 10^{-2} \), increasing
from 2 per cent in the most inefficient star-forming galaxies to 
\sim 20 per cent. In galaxies with higher values of \( f_s \), the escape fraction rapidly increases to nearly unity in galaxies with \( f_s \gtrsim 0.1 \). This makes physical sense because if a large fraction of gas forms stars, then there will be more ionizing photons per baryon in the halo, accelerating the ionization of the ISM and thus the escape of any ionizing radiation. Inspecting Fig. 4, only the lowest mass galaxies exhibit such high efficiencies. The scatter in this relation is caused by the variations in the halo’s star formation history and environment. The behaviour of \( f_{\text{esc}} \) with respect to sSFR shows no apparent trend, and most of the galaxies \( f_{\text{esc}} \) values lie between 2 and 40 per cent.

### 3.4.3 Time-dependent behaviour and correlation with star formation rates

So far, we have focused on the star-forming properties and UV escape fractions independent of time. However, galaxies are very dynamic with widespread turbulence, \( \text{H} \text{II} \) regions growing and then recombing, and SNe blast waves propagating through the ISM all occurring while the halo hierarchically grows. To explore the time dependence of the escape fraction, we focus on the most massive halo that grows from \( 2.2 \times 10^8 \) to \( 5.5 \times 10^8 \) M\(_{\odot}\) during the last 80 Myr of the simulation. The lower-left panel in Fig. 10 shows the escape fraction, SFR, and halo mass as a function of time, starting at \( z = 8 \). The remaining panels in Fig. 10 show projections of density-weighted gas density and average UV flux at \( E = 21.6 \) eV inside of this halo at 10 Myr intervals.

This galaxy can sustain star formation at all times, and it experiences two epochs of stronger star formation. At \( z = 8 \), the SFR is \( 1.1 \times 10^{-2} \) M\(_{\odot}\) yr\(^{-1}\), which then increases to \( 2.5 \times 10^{-2} \) M\(_{\odot}\) yr\(^{-1}\) 20 Myr later and then decays as the cold dense gas is disrupted inside the galaxy. Afterwards the gas cools again and re-collapses to produce a slightly weaker burst of star formation at \( 2.0 \times 10^{-2} \) M\(_{\odot}\) yr\(^{-1}\), and it subsequently steadily decreases to \( 0.8 \times 10^{-2} \) M\(_{\odot}\) yr\(^{-1}\) at the end of the simulation.

These two bursts of star formation induce a spike in \( f_{\text{esc}} \), which is clearly seen in Fig. 10. Before the first burst, the escape fraction varies around 0.01, and then once the burst occurs, it rapidly increases to 0.13 as the \( \text{H} \text{II} \) region partially breaks out of the

#### Table 4. UV escape fractions as a function of star formation efficiency and sSFR.

| log\( f_s \) | \( f_{\text{esc}} \) |
|---|---|
| − 3.75 | 0.02\(^{\pm}\)0.00 |
| − 3.25 | 0.12\(^{\pm}\)0.06 |
| − 3.75 | 0.26\(^{\pm}\)0.13 |
| − 2.25 | 0.20\(^{\pm}\)0.04 |
| − 1.75 | 0.34\(^{\pm}\)0.20 |
| − 1.25 | 0.81\(^{\pm}\)0.18 |
| − 0.75 | 0.99\(^{\pm}\)0.00 |

\( f_{\text{esc}} \) values lie between 2 and 40 per cent. In galaxies with higher values of \( f_s \), the escape fraction rapidly increases to nearly unity in galaxies with \( f_s \gtrsim 0.1 \). This makes physical sense because if a large fraction of gas forms stars, then there will be more ionizing photons per baryon in the halo, accelerating the ionization of the ISM and thus the escape of any ionizing radiation. Inspecting Fig. 4, only the lowest mass galaxies exhibit such high efficiencies. The scatter in this relation is caused by the variations in the halo’s star formation history and environment. The behaviour of \( f_{\text{esc}} \) with respect to sSFR shows no apparent trend, and most of the galaxies \( f_{\text{esc}} \) values lie between 2 and 40 per cent.

#### 3.5 Clumping factor

Once ionizing radiation escapes into the IGM, it can create a cosmological \( \text{H} \text{II} \) region. To remain ionized, the ionization rate must be greater than the recombination rate (RR). Recombination in a clumpy IGM is accelerated in overdense regions because its rate is proportional to the product of the electron and proton number densities, \( n_e n_p \). This enhancement factor is generally characterized by the clumping factor \( C \) that is traditionally defined as \( C \equiv \langle \rho^2 \rangle / \langle \rho \rangle^2 \), where the brackets indicate a volume average. Finlator et al. (2012, hereafter F12) explored the variance of \( C \) with its definition, whether it is calculated as

(i) the clumping of all baryons above some threshold density to delineate between collapsed objects and the IGM, 
(ii) the clumping of electrons and protons,

\[
C_{\text{H} \text{II}} \equiv \frac{(n_e n_{\text{H} \text{II}})}{(n_e)(n_{\text{H} \text{II}})},
\]

that can be computed in only ionized regions or be weighted by the ionized volume fraction \( x \) (see section 3 in F12 for a discussion),

(iii) a clumping factor that improves method (ii) by using the RR \( \alpha_0(T) \) at the temperature of the simulated gas (Shull et al. 2012) and is also weighted by \( x \),

\[
C_{\text{H} \text{II,RR}} \equiv \frac{(n_e n_{\text{H} \text{II}} \alpha_0(T))}{(n_e)(n_{\text{H} \text{II}})(\alpha_0(T))},
\]

(iv) an ‘observational temperature-corrected’ clumping factor of ionized gas that modifies method (iii) by replacing the RR in the denominator with the value at \( T = 10^4 K \) because the observed mean IGM temperature is poorly constrained in ionized regions,

\[
C_{\text{H} \text{II,10^4K}} \equiv \frac{(n_e n_{\text{H} \text{II}} \alpha_0(T))}{(n_e)(n_{\text{H} \text{II}})(\alpha_0(10^4K))}.
\]

F12 find that the clumping factor is sensitive to its definition, varying in the range 2–4 at \( z = 6 \). We find similar variations, and we show them in Fig. 11, which depicts the evolution of \( C \), two definitions.
Figure 10. Lower left: the evolution of the UV escape fraction (top panel), SFR (middle panel), and halo mass (bottom panel) of the most massive halo, starting at $z = 8$. Remaining panels: projections of density-weighted gas density (left-hand column) and average UV ($E = 21.6$ eV) flux (right-hand column) of the most massive halo every 10 Myr, starting at 660 Myr, which are marked in the time-evolution plot. These projections show the variance of the gaseous structure in the galaxy and the directions in which UV radiation can escape from the halo. The projections have a field of view of 6 proper kpc and a depth of 600 proper pc. The circles show the virial radius at each time.
of $C_{\text{Hen}}$, $C_{\text{Hen},10^4 \, \text{K}}$, the fit from F12,

$$x_{\text{Hen},C_{\text{Hen},10^4 \, \text{K}}} = 9.25 - 7.1 \log_{10}(1 + z)$$

and the $C_{\text{Hen}}$ fit ($z \sim 10.5$ reionization case) from Pawlik, Schaye & van Schepenzeel (2009),

$$C_{\text{Hen}} = \begin{cases} 
1 + \exp(-0.28z + 3.59) & (z \geq 10) \\
3.2 & (z < 10)
\end{cases}$$

For all of these definitions of $C$, we restrict our analysis to the diffuse IGM with $\rho/\rho_c < 20$.

We show two definitions of $C_{\text{Hen}}$, where $C_{\text{Hen}}$ is weighted by the ionized fraction $x$, and $C_{\text{Hen},2}$ is the clumping factor for partially ionized ($x > 0.1$) gas. All definitions of $C$ in the ionized regions generally increase from 1.5 to 3 from redshift 15 to 7.2, agreeing with other works (Pawlik et al. 2009; McQuinn, Oh & Faucher-Giguère 2011; F12; Shull et al. 2012; So et al. 2014). The evolution of $C_{\text{Hen},2}$ shows two abrupt increases at $z \sim 11$ and 9 followed by little evolution over the next $\sim 100$ Myr. Both occur when a galaxy quickly ionizes the surrounding several kpc during a star formation event that has a high $f_{\text{esc}}$, also apparent in the jumps in ionization fraction $x$ in Fig. 1. These events are more clear in $C_{\text{Hen}}$ and $C_{\text{Hen},10^4 \, \text{K}}$, where the sudden increases in $C$ occur when the H$\text{\textsc{ii}}$ region grows and encompasses overdensities that were previously neutral. After a sound-crossing time, these clumps photoevaporate, and the clumping factor decreases. These individual features are caused by the small simulation volume, where this behaviour in many different H$\text{\textsc{ii}}$ regions would average out, resulting in a smoothly increasing clumping factor. Our clumping factor is consistently higher than the F12 fit by $\sim 0.25$ on average because we resolve smaller systems above the cosmological Jeans mass that contribute to IGM clumpiness (Emerson, Thomas & Alvarez 2013).

### 4 REIONIZATION MODEL

Small-scale simulations have the benefit of higher resolution, but they cannot capture the formation of rare large-scale density peaks and the evolution of global reionization from a statistically complete sample of galaxies. Low-luminosity galaxies hosted in MC haloes should contribute a significant fraction of ionizing photons at very high redshifts because of their large number densities. On the other hand, they are susceptible to negative radiative feedback because these haloes can be photoevaporated from external UV radiation and their gas can be easily expelled by SN explosions. To assess the global impact of these smallest galaxies during reionization, we utilize the mean galaxy properties and escape fractions from our simulation in a semi-analytical model of reionization.

#### 4.1 Method

We compute the evolution of the hydrogen ionized fraction $x$ by solving

$$\dot{x} = \frac{n_y - x}{\tau_{\text{esc}}}$$

where $\dot{n_y}$ is the comoving moving photon emissivity, $\dot{n}_H$ is the mean comoving hydrogen number density, and $\tau_{\text{esc}} = [C(z)\eta_Y n_H(1 + Y/4X)(1 + z)^3]^{-1}$ is an effective recombination time for a fully ionized hydrogen gas (see So et al. 2014, for a discussion). $X = 0.76$ and $Y = 1 - X$ are the hydrogen and helium number fractions, respectively (Shapiro & Giroux 1987; Madau et al. 1999). We use the clumping factor $C_{\text{Hen}}$ from Pawlik et al. (2009, equation 10) and start with an initial ionized fraction of $10^{-3}$ at $z = 30$. We integrate this equation until the volume is completely ionized, giving a full reionization history from which we can calculate the optical depth due to Thomson scattering,

$$\tau_x = \int_0^{\infty} \frac{c(1 + z)^2}{H(z)} x(z) \sigma_T n_H(1 + n_Y/4X) \, dz,$$

where $H(z)$ is the Hubble parameter, $\sigma_T$ is the Thomson cross-section. We assume that the helium is singly ionized ($\eta = 1$) at $z > 3$ in the same volume fraction as hydrogen and doubly ionized ($\eta = 2$) at later times. Comparing the calculated $\tau_x$ of our models to the observed values from WMAP and Planck, $\tau_x = 0.089^{+0.012}_{-0.014}$, can place constraints on the timing of reionization and the ionizing emissivity.

#### 4.1.1 Ionizing emissivity

Most of the uncertainties are hidden in the ionizing photon emissivity (equation 3). For a halo mass independent model, $\dot{n}_Y = f_{\text{esc}} f_{\gamma} \dot{\rho}_s$, where $\dot{\rho}_s$ is the SFR density, and $f_{\gamma}$ is the photon to stellar baryon number ratio. However, we have shown that the escape fraction and SFRs are strong functions of halo mass $M$; therefore, we consider

$$\dot{n}_Y = \int_{M_{\text{min}}}^{\infty} f_{\text{esc}} f_{\gamma} (f_M f_{\text{vir}}) \, dM_{\text{vir}},$$

where all of the factors inside the integral are functions of halo mass, and the product inside the parentheses is the cosmic SFR density in halo masses between $M$ and $M + dM$. We take $M_{\text{min}} = 10^{6.25} M_\odot$ from our simulation. Here $f_M$ is the time derivative of the collapsed fraction that is calculated with the ellipsoidal variant of Press–Schectcher formalism (Press & Schechter 1974; Sheth, Mo & Tormen 2001) with the same cosmological parameters used in the simulation.
We compute $\dot{n}_\gamma$ by discretizing the integral in equation (13) into mass bins of log $(M_{\text{vir}}/M_\odot) = 0.5$ in log $(M_{\text{vir}}/M_\odot) \in [6.25, 12.75]$. At log $(M_{\text{vir}}/M_\odot) < 8.75$, we utilize the luminosity-weighted mean values of $f_{\gamma\text{esc}} f_{\gamma\text{int}}$ from the simulation (Table 3). For more massive haloes that are not sampled by our simulation, we assume a mass-independent values (cf. Alvarez et al. 2012), $(f_{\gamma}, f_{\gamma\text{esc}}, f_{\gamma\text{int}}) = (0.03, 0.05, \Omega_b/\Omega_m)$.

Metal-poor stars can produce up to a factor of 2 more ionizing photons per stellar baryon, compared to their solar metallicity counterparts, because of higher surface temperatures. To account for this effect, we utilize the photon to stellar baryon ratio $n_{\gamma}/n_{\text{baryon}}$ from Schaerer (2003, their equation 1). Then we can express $f_{\gamma} = f_\gamma(Z(M_{\text{vir}}))$ through two relations: (i) the local dwarf galaxy metallicity–luminosity relation (Woo, Courteau & Dekel 2008),

$$\log(Z) = -3.7 + 0.4 \log \left( \frac{M_{\text{vir}}}{10^6 M_\odot} \right),$$

and (ii) our simulated $M_{\text{vir}} - M_{\text{esc}}$ mean values (Table 1), resulting in a decreasing $\gamma$ with increasing $M_{\text{vir}}$.

Lastly, we include emissivity from Pop III stars in one model. They only form in metal-free haloes that are susceptible to LW feedback and metal enrichment. Simulations that include these physics show the SFR increasing for the first ~100 Myr, and afterwards the SFR becomes approximately constant prior to reionization (e.g. Wise et al. 2012b; Xu, Wise & Norman 2013). Therefore, we assume a constant Pop III SFR of $5 \times 10^{-3} M_\odot \text{yr}^{-1} \text{Mpc}^{-3}$, starting at $z = 30$, with $f_{\gamma_{\text{esc}}} = 60 000$ (Schaerer 2002). This corresponds to $n_{\gamma} = 1.1 \times 10^{50} \text{s}^{-1} \text{cm}^{-3}$. Note that this emissivity does not enter the integral in equation (13) but adds a constant term to $\dot{n}_\gamma$.

### 4.1.2 Dwarf galaxy suppression

The suppression of star formation occurs in low-mass haloes that are susceptible to negative feedback through photodissociation, gas blowout, and/or photoevaporation. We showed in Fig. 3 that the halo–galaxy occupation fraction $f_{\text{host}}$ decreases from an initial value $f_0$ to a final value $f_1$ after a sound-crossing time (cf. Shapiro et al. 2004; Sobacchi & Mesinger 2013)

$$t_s \approx 200 \text{Myr} \left( \frac{M}{10^8 M_\odot} \right)^{1/3} \left( \frac{1+z}{10} \right)^{-1} \left( \frac{\Omega_\text{b}h^2}{0.15} \right)^{-1/3}.$$

We apply this suppression when the filtering mass $M_{\gamma}(t_\gamma) > M_{\text{esc}}$ by multiplying $\dot{n}_\gamma$ by

$$f_{\text{host}}(M, t) = A - B \tanh \left( \frac{t - t_{\gamma} - t_{\text{esc}}/2}{t_{\text{esc}}/3} \right),$$

where $A = (f_0 + f_1)/2$ and $B = (f_0 - f_1)/2$, which provides a functional fit to the simulated values of $f_{\text{host}}$ that are shown in Fig. 3.

To calculate the filtering mass (equation 2), we use a simple model that uses the Jeans mass $M_J$ of an ionized IGM with $T = 10^4$ K and $\rho = \Omega_\text{b}h^2$.

Fig. 3 shows that star formation is suppressed in galaxies that cannot cool through atomic transitions. Thus, we only use this transition for the mass bins centred on log $(M_{\text{vir}}/M_\odot) = [7.0, 7.5, 8.0]$, where we use $f_0 = (0.3, 0.5, 1.0)$ and $f_1 = (0.01, 0.15, 0.5)$, respectively. For log $(M_{\text{vir}}/M_\odot) = 6.5$, we use $f_{\text{host}} = 2.4 \times 10^{-4}$, the time-averaged value, because these extremely low-mass galaxies are sporadic and rare (see Section 3.2). Lastly, we do not alter the emissivities of the atomic cooling haloes with log $(M_{\text{vir}}/M_\odot) > 8.25$.

### 4.2 Results

Here we consider three models that progressively add more ionizing radiation sources: (i) star formation only in haloes with masses $M_{\text{vir}} > 10^{6.25} M_\odot$ that are approximately atomic cooling haloes, (ii) plus star formation in minihaloes with masses $M_{\text{vir}} > 10^{6.25} M_\odot$, and (iii) plus Pop III star formation. Fig. 12 shows the main results from our semi-analytic reionization models.

The model that restricts star formation to atomic cooling haloes reions the Universe at $z = 5.5$, resulting in $\tau_e = 0.059$, which is typical of models either only considering atomic cooling haloes with low escape fractions that are similar to local dwarf galaxies or only including observable galaxies at $z \gtrsim 6$ (e.g. see the $M_{\text{vir}} = 17$ model of Robertson et al. 2013). To explain the discrepancy between the observed values of $\tau_e$ and the models that include only currently observable galaxies, high escape fractions may be invoked (e.g. Alvarez et al. 2012; Kuhlen & Faucher-Giguère 2012; Robertson et al. 2013) and other sources of ionizing photons, such as X-ray binaries (Fragos et al. 2013; Power et al. 2013) and Pop III stars (Ahn et al. 2012). Kuhlen & Faucher-Giguère and Robertson et al.
both used a mass-independence description of the star formation efficiency and escape fraction, but Alvarez et al. presented a simple model that delineated between low- and high-mass dwarf galaxies with \( f_{\text{esc}} = 0.8, 0.05 \), respectively. None of these recent studies considered minihaloes because they are very susceptible to negative feedback; however, our simulation shows that they can indeed form a non-negligible amount of stars with high escape fractions.

Our model (ii) includes such low-luminosity galaxies, which boosts \( \tau_r \) to 0.0939 that is very close to the best-fitting value from Planck of \( \tau_r = 0.0925 \) illustrated in the middle panel of Fig. 12. This model reionizes the Universe at \( z = 6.4 \). The bottom panel of Fig. 12 shows that the ionizing photon emissivity is already \( 2 \times 10^{40} \text{s}^{-1} \text{cMpc}^{-3} \) when minihaloes are not included. It continues to rise until it reaches \( 8 \times 10^{40} \text{s}^{-1} \text{cMpc}^{-3} \) at \( z \sim 10 \). Eventually these galaxies are photosuppressed, and the total ionizing emissivity converges to model (i) at \( z \sim 6 \) that are consistent with observational constraints (Kuhlen & Faucher-Giguère 2012; Becker & Bolton 2013). These smallest galaxies have \( f_{\text{esc}} \sim 0.5 \), and their host haloes collapse much earlier than the atomic cooling haloes, leading to the boost at very high redshifts. The top panel of Fig. 12 shows that this early time behaviour produces a more extended reionization history with an ionized volume fraction of \( x = 0.2 \) by \( z = 14 \) and \( x = 0.5 \) by \( z = 9.4 \). The top panel of Fig. 13 shows the instantaneous fractional emissivity from haloes below three different mass thresholds that are often used for suppression, \( T_{\text{vir}} = 10^4 \text{K}, V_c = 30 \text{Kms}^{-1}, \) and \( M_{\text{vir}} = 2 \times 10^9 \text{M}_\odot \). The MC haloes provide 75 per cent of the ionizing emissivity at \( z = 15 \), dropping to 10 per cent by \( z = 7 \), as they are photosuppressed, and larger galaxies are the main source of reionization at later times. Similar trends are seen in the other two halo mass thresholds, where at \( z = 10 \), haloes with \( V_c \lesssim 30 \text{Kms}^{-1} \) and \( M_{\text{vir}} \lesssim 2 \times 10^9 \text{M}_\odot \) produce 50 and 80 per cent of the ionizing emissivity, respectively. The bottom panel of Fig. 13 shows the cumulative fraction of ionizing radiation that originates from haloes below the same halo mass thresholds. The key point to take from these results at \( z = 6 \) is that 27, 36, and 56 per cent of the total ionizing photon budget are created in haloes with \( T_{\text{vir}} \leq 10^4 \text{K} \), \( V_c \leq 30 \text{Kms}^{-1} \), and \( M_{\text{vir}} \leq 2 \times 10^9 \text{M}_\odot \), respectively. Thus, we conclude that the lowest luminosity galaxies play an integral role in the reionization of the Universe but are eventually suppressed as they are engulfed by an increasing UV radiation field.

Short-lived Pop III stars provide an additional source of ionizing photons, where they ionize the surrounding few kpc, and then this \( \text{H}_i \) region quickly recombines. However in our model, they have a low-level contribution to the ionizing photon budget, increasing the \( n_{\text{esc}} \) by \( 1.1 \times 10^{50} \text{s}^{-1} \text{cMpc}^{-3} \). This increases \( \tau_r \) to 0.106 that is in the upper 1 \( \sigma \) bound of the Planck results and results in complete reionization at \( z = 6.9 \).

For mass-independent models of reionization, it is useful to consider luminosity-weighted mean value of \( f_{\text{esc}} \) and the host halo mass, which are shown as a function of redshift in Fig. 14. At early times, the low-luminosity galaxies are not suppressed and are the biggest sources of the ionizing photon budget, which is apparent by the mean halo mass of \( 10^{7.2} \text{M}_\odot \) and \( f_{\text{esc}} = 0.46 \) at redshift 20. As these galaxies are suppressed, the halo mass scale increases to \( 10^{8.6} \text{M}_\odot \) by redshift 6 while the mean escape fraction gradually drops to \( f_{\text{esc}} = 0.05 \), which is the assumed escape fraction of these larger galaxies. This time-dependent behaviour is generally true for any model that considers multiple galaxy populations that are suppressed and unaffected by feedback mechanisms (cf. Alvarez et al. 2012); however, the evolution of \( f_{\text{esc}} \) is much slower than the one assumed in Haardt & Madau (2012) as shown in Fig. 14.

Our results are well fitted by analytic functions and can be easily utilized in reionization models. Fitting the time dependence of \( f_{\text{esc}} \) with a pure Gaussian had errors up to 20 per cent at early times and is better fitted with a Voigt profile,

\[
\langle f_{\text{esc}}(z) \rangle = 0.54 - 544(G(z, \sigma, z_0) L(z, \Gamma, z_0)),
\]

where \( G \) and \( L \) are Gaussian and Lorentzian distribution functions that are normalized to unity, respectively. Our best-fitting model has \( \sigma = 19.6, \Gamma = 7.26 \), and \( z_0 = 5.8 \) and is only valid for \( z > z_0 \). Prior to reionization, the luminosity-weighted halo mass scale

\[
M_{\text{vir}} = 10^9 \text{M}_\odot
\]
asymptotes to linear relations at early and late times and can be fit by a rotated hyperbola. But for computational convenience, we can fit the behaviour with

$$\log(M_{\text{fit}}(z)) = 7.0 + (0.25 + 2.96 \times 10^{-4}z^{3.16})^{-1}. \quad (18)$$

Both fits are good to within 3 per cent at \(z > 5.8\), where our \(f_{\text{esc}}(z)\) fit reaches a minimum. These fits encapsulate the effects of suppression of the lowest mass dwarf galaxies that have high escape fractions. Coupled with our mass-dependent dwarf galaxy properties presented in Section 3, this resulting reionization history demonstrates the role of high-redshift, photosuppressible dwarf galaxies during reionization.

5 DISCUSSION

We have demonstrated that low-luminosity galaxies play a key role during the early phases of reionization. The exact properties of a particular high-redshift dwarf galaxy most critically depend on the star formation history and the ionization and thermal properties of its local environment. For instance, the magnitude of radiative and SN feedback in their progenitors will regulate the gas and metal content of the galaxy, thus affecting the strength of radiative cooling and star formation in the dwarf galaxy.

As previous studies have shown (e.g. Clarke & Oey 2002; Wise & Cen 2009; Fernandez & Shull 2011; Benson et al. 2013), ionizing radiation mainly escapes through low-density channels that are created by ionization fronts or SNe. The location and strength of star formation and galaxy morphology can both influence the UV escape fraction. Thus, resolving star-forming clouds and the multiphase ISM are necessary requirements for any simulation that aims to measure the escape fraction. Furthermore, environmental properties, in particular, the incident radiation can affect the formation of the first galaxies and their escape fractions. First, any LW radiation will suppress \(H_2\) formation and thus Pop III stars in the progenitors. If Pop III star formation is delayed until haloes have \(M \gtrsim 10^7 M_\odot\), the \(H\alpha\) region and SN blast wave may fail to breakout of the halo, possibly leading to prompt metal-enriched star formation (Whalen et al. 2008; Ritter et al. 2012). Secondly, any external ionizing radiation will photoevaporate the gas in low-mass haloes over a sound-crossing time. However, photoevaporation may boost the escape fraction for a short period if the halo is already hosting active star-forming regions. If the outer layers of gas are photoevaporated by an external source, the neutral hydrogen column density between the halo centre and the IGM will decrease, causing an increase in escape fraction in principle. On the other hand, this reduces the amount of gas available for future star formation in small galaxies. If the halo does not accrete additional gas from smooth accretion or a merger within a sound-crossing time, the SFR and escape fraction will steadily decrease, where we showed a similar case of a correlation between SFR and escape fraction in Fig. 10.

Although the SFRs in the lowest mass galaxies are small, their roles in reionization are not insignificant. Now we turn our attention to the implications of our results on reionization, their observational prospects, differences with previous work, and caveats of our study.

5.1 Implications for reionization

The idea of the faintest galaxies providing the majority of the ionizing photon budget of reionization is not a new one. However, our work provides convincing evidence that stars form in these galaxies before becoming photosuppressed by internal stellar feedback and external radiative feedback. Their star formation efficiencies are not significantly lower than atomic cooling haloes, but their low masses lead to low SFRs of \(10^{-3} - 10^{-4} M_\odot\) yr\(^{-1}\) with about half of the ionizing radiation escaping into the IGM. Combined with a high number density of their host haloes, their contribution to reionization should not be neglected, especially at very high redshift \((z \gtrsim 10)\). Some of these galaxies are initially embedded in a cool and neutral ISM, most likely in a relic \(H\alpha\) region from Pop III stars, but as global reionization proceeds, they are likely embedded in larger \(H\alpha\) regions, slowly being photoevaporated over a sound-crossing time. Then larger galaxies that are hosted by atomic cooling haloes provide the majority of ionizing radiation, as shown in Fig. 14. In a statistical sense, there will probably be no detectable transition in the reionization or SFR history between these two source types because they form coeval. A significant fraction of galaxies that are initially photosuppressed will likely host star formation shortly afterward because rapid mass accretion rates at high redshift will allow for efficient cooling and star formation even in the presence of a UV radiation field.

This scenario leads to an extended period of reionization, where the Universe has an ionized mass fraction of 10 and 50 per cent by \(z \sim 17\) and \(z \sim 10\), respectively, eventually becoming completely reionized by \(z \sim 6.5\) (see Fig. 12). Such an extended ionization history produces a Thomson scattering optical depth \(\tau_e = 0.093\) and an ionizing emissivity that are consistent with Planck and Ly\(\alpha\) forest observations, respectively. We stress that the faintest galaxies should not be overlooked in reionization models and provide the key to matching the latest ionization constraints, resolving any tension between CMB observations and Ly\(\alpha\) forest observations at \(z \sim 6\).

5.2 Observational prospects

Fig. 15 shows the absolute magnitude at 1500 Å of a typical dwarf galaxy that contributes to reionization as a function of redshift.

![Figure 15](http://mnras.oxfordjournals.org/)

Figure 15. Absolute UV magnitude at 1500 Å for the typical dwarf galaxy contributing to reionization. The solid line uses the mean \(M_\star - M_{\text{vir}}\) relation shown in Table 1 to convert the luminosity-weighted average halo mass in Fig. 14, where the shaded areas show the 1σ deviations. The dashed lines extrapolate to halo masses \(M \gtrsim 10^5 M_\odot\). The thin dotted lines show the apparent magnitude that are denoted above the lines, where we have assumed a constant K-correction of –2. The solid green lines delineate the detection limits for the HUDF12 (\(M_{\text{lim}} = 30.1\)), Frontier Fields (\(M_{\text{lim}} = 28.7 + 2.5\log \mu\)), and JWST ultradepth (\(M_{\text{lim}} = 31.4\)) campaigns, where \(\mu\) is the magnification factor. Lastly, the magenta squares show the galaxies observed in the HUDF12 campaign from the McLure et al. (2013) \(z \geq 6.5\) robust sample.
redshift and compare them to the detection limits of the HUDF12, Frontier Fields, and JWST ultradeep campaigns. Here we take the luminosity-averaged halo mass, shown in Fig. 14 and show the average and 1σ deviations of $M_{UV}$ from Table 1. Even at $z < 10$, the continuum radiation from these typical galaxies is below the detection limits in the HUDF12 campaign. However, with sufficient magnification from gravitational lensing, observations from the Frontier Fields may detect such a galaxy population that contributes the majority of radiation to reionization (e.g. Mashian & Loeb 2013; Coe, Bradley & Zitrin 2014).

Recall that our calculation of $M_{UV}$ only considers stellar radiation and not nebular emission. In particular, Lyα emission from the HII region will be strong in these galaxies, perhaps having an intrinsic equivalent width (EW) as high as 1500 Å (Schaerer 2002; Johnson et al. 2009; Dijkstra & Wyithe 2010). In a static ISM/IGM, Lyα photons would be absorbed by the surrounding neutral medium. However, Dijkstra & Wyithe (2010) showed that a $\gtrsim 50$ km s$^{-1}$ H1 outflow allows for 10–20 percent of the Lyα emission to be transmitted through a neutral IGM, still resulting in a strong EW of $\sim 100$ Å (see also Verhamme, Schaerer & Maselli 2006; Verhamme et al. 2008). Inspecting the most massive galaxy in our simulation at redshifts 12 and 7.3, we find that the intrinsic log $L_{\text{Ly}\alpha} = (37.3, 40.3)$ erg s$^{-1}$ in a sphere of radius 2$r_{200}$, assuming that all ionizing radiation is absorbed by the nearby neutral IGM. This is comparatively higher than log $L_{\text{Ly}\alpha} = (36.0, 39.0)$ erg s$^{-1}$ from stellar emission alone. At these respective redshifts, the galaxy has a total mass of $2.7 \times 10^{7}$ M$_{\odot}$ and $6.8 \times 10^{8}$ M$_{\odot}$ and a stellar mass of $1.5 \times 10^{6}$ M$_{\odot}$ and $3.5 \times 10^{7}$ M$_{\odot}$. Outflows are ubiquitous in high-redshift dwarf galaxies, and we thus expect that a significant fraction of Lyα emission would be transmitted through the IGM. We intend to follow-up the observable Lyα line profiles and strengths in a more complete statistical sample of high-redshift galaxies presented in Xu et al. (2013).

Even with the exquisite sensitivity of JWST, the typical reionizing sources will not be detectable. Only galaxies with an SFR $> 0.1$ M$_{\odot}$ yr$^{-1}$ will be detected in 10$^6$ s exposures (Pawlik et al. 2013). However, surveys of gravitational lensed regions may uncover a significant fraction of such galaxies, for instance, median magnifications are between 2 and 15 in the CLASH fields (Bouwens et al. 2012b; Bradley et al. 2013). Searches with narrow-band filters at a particular redshift around the Lyα $\lambda 1215$, He II $\lambda 1640$, and Hα $\lambda 6536$ lines (e.g. Johnson et al. 2009; Paardekooper et al. 2013) in gravitational lensed fields may be the best strategy for detecting high-redshift dwarf galaxies (e.g. Zackrisson et al. 2012). If detected, these faint galaxies would be highly obscured because the majority of the radiation would be propagating through ionized channels in the ISM and surrounding IGM. Would they constitute a new galaxy class that only exist prior to cosmic reionization, existing in large-scale neutral regions of the Universe embedded in their own HII region? Because of their unique environment, they would have no direct present-day analogue, and models that include radiative Pop III and II/I stellar feedback, creating local HII regions and outflows are necessary to make solid predictions of the connection between their intrinsic and observable properties.

5.3 Comparison to previous work

5.3.1 Star formation rate and efficiency

W12 found that the mean stellar metallicity and its distribution function were good discriminates of a plausible star formation and feedback implementation, avoiding the typical galaxy formation simulation ‘overcooling problem’. Little is published on simulated stellar metallicity data in the first galaxies (however, see Ricotti & Gnedin 2005), so we will compare the SFRs and efficiencies to previous work.

Ricotti, Gnedin & Shull (2008) found a power-law dependency between halo mass and star formation efficiency with a slope of 1.5 and 2 in their weak and strong feedback cases in their cosmological radiation hydrodynamics simulations of early galaxy formation. In their weak case, log$f_{\text{SFR}} \simeq -3.0$ and $-1.5$ at halo masses of $10^7$ and $10^8$ M$_{\odot}$, respectively. We see no such trend in $f_{\text{SFR}}$ (see Fig. 4), where we find a decreasing trend at $M \lesssim 10^9$ M$_{\odot}$ with a large scatter because the outflows from the initial star formation event temporarily suppresses any further star formation. At larger masses it slowly increases to 1–3 per cent at $M = 10^{10.5}$ M$_{\odot}$, where we would expect it to plateau at higher halo masses. It is wise to disregard their power-law fit at higher masses because it diverges, and the star formation efficiency probably levels out at higher masses (see Pawlik et al. 2013).

We find acceptable agreement with the low-mass haloes in the ‘LW+RT’ simulation of Pawlik et al. (2013) that considered most of the physics included in our simulation with the exception of a model of Pop III star formation and feedback, metal cooling, and radiation pressure. However, they include the effects of stellar radiative feedback in their work, which plays a significant role in regulating star formation in these low-mass galaxies. They find log$f_{\text{SFR}} \simeq -3.0$, slightly lower than our results, which could come from the lack of metal cooling, resulting in lower cooling rates and thus star formation efficiencies. On the other hand, there are similarities between our results, in that, they have a similar scatter and no dependence on halo mass. Their values of $f_{\text{SFR}}$ increase rapidly to $\sim 0.1$ when it can atomically cool, which is about a factor of 5 higher than our results. Lastly, they find similar gas fractions $f_{\text{gas}} \gtrsim 0.1$ that are depressed in low-mass haloes.

Biffi & Maio (2013) analysed a cosmological simulation that samples mostly MC haloes (up to $7 \times 10^7$ M$_{\odot}$ at $z = 9$) and includes distinct models of Pop III and Pop II/I star formation. In their $z = 9$ data, they find a suppressed gas fraction of 2–5 per cent in haloes with $M \sim 10^8$ M$_{\odot}$, rising to 10 per cent in $\sim 10^7$ M$_{\odot}$ haloes. We find a similar suppression, but the haloes only recover to $f_{\text{gas}} = 0.1$ in $10^6$ M$_{\odot}$ haloes. We suspect that their elevated gas fractions result from the lack of radiative feedback. Star formation is suppressed below a halo mass scale of $5 \times 10^6$ M$_{\odot}$, agreeing with our results. In haloes with $M \gtrsim 10^7$ M$_{\odot}$, they find stellar mass fractions ($M_{\star}/M_{\text{halo}}$) between $10^{-5}$ and $10^{-4}$. The stellar mass fractions in our work in these haloes are in the range $1–4 \times 10^{-4}$. Their objects with high star formation efficiencies most probably arises from the higher gas fractions. They also find a population of haloes with a very small $f_{\text{SFR}} = 10^{-6}–3 \times 10^{-5}$, which is below our stellar mass resolution of 1000 M$_{\odot}$.

5.3.2 UV escape fraction

In the past five years, theoretical work has favoured high escape fractions between 0.1 and 0.8 from galaxies with total masses $M \lesssim 10^8$ M$_{\odot}$ (Wise & Cen 2009; Razoumov & Sommer-Larsen 2010; Yajima et al. 2011; Paardekooper et al. 2013). We also find high average $f_{\text{esc}}$ values of $\sim 0.5$ but only in haloes with $M \lesssim 2 \times 10^7$ M$_{\odot}$, which are then photosuppressed. The UV escape fraction steadily decreases with increasing halo mass to a luminosity-weighted average of 25 and 5 per cent for $10^8$ M$_{\odot}$ and $10^{8.5}$ M$_{\odot}$ haloes, respectively.
Why do we find lower escape fraction in low-mass atomic cooling haloes than other recent studies? To explain this, we can describe the shortcomings of Wise & Cen (2009), who extracted haloes from cosmological simulations without radiative cooling, star formation, and feedback as initial conditions. These haloes had a gas fraction near the cosmic mean, which then proceeded to monolithically collapse because radiative cooling was immediately activated in their high-resolution re-simulations. This produced unrealistically strong starbursts in their 10 halo samples with star formation efficiencies of 5–10 percent and \( f_{\text{esc}} \approx 0.4 \) for haloes with \( M \gtrsim 10^6 \, M_\odot \). For such strong starbursts, we found that \( f_{\text{esc}} \gtrsim 0.5 \) (see Fig. 9 and Table 4). Because the \( M = 10^8 - 10^9 \, M_\odot \) haloes in Razoumov & Sommer-Larsen (2010) and Yajima et al. (2011) were the smallest in their sample, they would have suffered the same aberration, which is a general consequence of missing early phases of galaxy formation, leading to the overcooling problem. If the haloes were allowed to form stars throughout their assembly, then the SFRs and efficiencies would have been regulated over this period, leading to more controlled star formation events and lower \( f_{\text{esc}} \) values. Analogous behaviour for the escape fraction was seen in the metal cooling analyses, where they consider all star clusters and whereas we only consider young (< 30 M\(_\odot\)) stars. As the haloes are photoevaporated, the ionized fraction increasing from \( \sim 10^{-3} \) to nearly unity at \( z \approx 10 \), resulting in an SFR that is an order of magnitude higher than the RP simulation, which is presented here, that proceeded to reionize nearly the entire simulation volume. Recently using radiation hydrodynamics simulations, Kimm & Cen (2014) have found that the time-averaged mean escape fraction 10–15 percent in high-z dwarf galaxies hosted in haloes with \( 10^8 \lesssim M/\, M_\odot \lesssim 10^{10.5} \), which combined with our results may provide an accurate estimate of \( f_{\text{esc}} \) in galaxies that contribute substantially to reionization.

Our results for \( M \sim 10^7 \, M_\odot \) haloes are similar to the results of Pardekooper et al. (2013) before their uniform UV background activates at \( z = 12 \). Then their average \( f_{\text{esc}} \) values increase from \( \sim 0.06 \) to nearly unity at \( z = 6 \). Similar evolution occurs in \( 10^8 \, M_\odot \) haloes, increasing from \( \sim 0.4 \) to 0.95. We suspect that variations in our analyses, where they consider all star clusters and whereas we only consider young (< 20 Myr) star clusters, have caused the discrepancy between our two efforts. As the haloes are photoevaporated by the UV background at later times in their simulation, the UV stellar radiation from the older stars can escape more easily through a lower neutral column density, causing higher \( f_{\text{esc}} \) values at later times. They also see a similar but more abrupt transition from MC to atomic cooling haloes as the primary source of ionizing photons as the former objects are photosuppressed.

5.3.3 Reionization history

The inclusion of galaxies that are liable to photosuppression into a reionization model produces an extended reionization history with the ionized fraction increasing from \( x = 0.2 \) at \( z = 14 \) to \( x = 0.5 \) at \( z = 9 \), and finally becoming completely reionized by \( z \approx 6.5 \). This history is a consequence of a halo mass dependent escape fraction and SFRs, extending down to \( 10^6 \, M_\odot \) haloes that are drastically photosuppressed. It is very similar to the one presented in Haardt & Madau (2012), but the evolution of \( f_{\text{esc}} \) and the cosmic SFRs are much different in nature. Because galaxies can form in MC haloes, non-negligible SFRs extend to \( z \sim 15–30 \), reducing the need for an escape fraction of unity at \( z > 12.5 \) in their model. Recently a few groups (Kuhlen & Faucher-Giguère 2012; Shull et al. 2012; Robertson et al. 2013) calculated a reionization history that was based on the latest HUDF data, extrapolating the LF down to various limiting magnitudes, where they considered various constant values of \( f_{\text{esc}} \) and a redshift-dependent escape fraction. In a recent analysis of ancient stars in local dwarf galaxies, Salvadori et al. (2014) found a similar reionization history as the aforementioned works, but they concluded that galaxies in haloes with \( 10^7 \lesssim M/\, M_\odot \lesssim 10^9 \) can reionize 50 percent of a Milky Way environment by \( z \approx 8 \). Our reionization history is more extended than these works, where the difference comes from low-luminosity galaxies contributing more at higher redshifts. Their resulting \( \tau_e \) is still consistent with the latest WMAP and \( \text{Planck} \) data but on the low end of the 1σ errors.

Our reionization model uses a similar approach as Alvarez et al. (2012) with \( f_{\text{esc}} \) and \( f_{\text{esc}} \), being halo mass dependent, however, we use values that are calibrated from our simulation with six mass ranges instead of two. Their idea of a low-mass galaxy population driving early reionization is plausible and is supported by our simulations. Like the aforementioned works, their reionization history is slightly shorter than our results, mainly arising from their model only considering haloes with \( M > 10^8 \, M_\odot \) as star forming. The general trends, such as a peak in ionizing emissivity and early-time and late-time asymptotes in the luminosity-averaged escape fraction, are found in our model, but clearly with different source parameters, the details have changed. Nevertheless, we find this type of reionization history to be most plausible, considering the findings in our simulation presented in this paper.

5.4 Caveats

Our simulations include most of the relevant physical processes in galaxy formation and its associated star formation and feedback, but there are still some shortcomings in our work. The simulation volume is only 1 comoving Mpc\(^3\), which misses the effects of large-scale reionization and rare peaks in the cosmological density field. This, however, does not diminish our findings of the properties of early dwarf galaxies because stellar feedback is the dominant factor in simulating realistic galaxies (e.g. W12; Hopkins et al. 2013; Stinson et al. 2013). The small volume does restrict our analysis to 32 dwarf galaxies and evaluating the galaxy properties independent of time. The approach of combining the data at all outputs misses any evolution in the galaxy properties, but we have included the time-dependent effects of photosuppression in our semi-analytic reionization model.

We have not considered the effects of relative streaming velocities (\( v_{\text{rel}} \sim 30 \, \text{kms}^{-1} \) at \( z \sim 1100 \)) between baryons and DM that arise during recombination (Tseliakhovich & Hirata 2010). This phenomenon only suppresses Pop III star formation in the smallest minihaloes with \( M \lesssim 10^6 \, M_\odot \) (Greif et al. 2011a; Tseliakhovich, Barkana & Hirata 2011; Naoz, Yoshida & Gnedin 2012; O’Leary & McQuinn 2012) and should not significantly change our results because the circular velocities of the galaxy host haloes are much larger than the streaming velocity at \( z < 20 \).

On the topic of the escape fraction, there are a few processes that we do not model. First, we cannot capture the possibility of runaway massive stars that may boost \( f_{\text{esc}} \) as these stars travel into the outskirts of the dwarf galaxy and into the IGM (Conroy & Kratter 2012) because we model metal-enriched star formation at the stellar cluster scale. Second, we do not include the partial ionization by X-ray radiation from X-ray binaries (McQuinn 2012; Fragos et al. 2013; Power et al. 2013) or miniquasars (e.g. Ricotti & Ostriker 2004b; Kuhlen & Madau 2005; Holley-Bockelmann, Wise & Sinha 2012; Grissom et al. 2014), which may contribute up to 10 percent of the optical depth to Thomson scattering. Finally, we consider a Salpeter IMF (\( dN/dM_\star \propto M_\star^{-2.35} \)) for metal-enriched
stars, whereas recent observations of ultrafaint dwarf galaxies have suggested that the IMF slope is more shallow at $\alpha = 1.2^{+0.4}_{-0.4}$ for Hercules and $\alpha = 1.3 \pm 0.8$ for Leo IV (Geha et al. 2013). The shallower slope implies that their progenitors hosted star formation that favours massive stars more than present-day star formation. Wise & Cen (2009) also found that a top-heavy IMF increases the escape fraction by $\Delta f_{\mathrm{esc}} = 0.27 \pm 0.17$ but also suppresses star formation by $\sim 25$ per cent in the MC haloes. Considering a shallower IMF may change our results slightly in the low-mass end that we investigated, but it is still uncertain under which conditions the IMF becomes more top-heavy (e.g. see differing results in Japann et al. 2009; Smith et al. 2009; Safranek-Shrader, Milosavljević & Bromm 2014). On a similar topic, we used a characteristic mass of 100 $M_\odot$ for our Pop III IMF, which is somewhat higher than recent Pop III star formation simulations that find characteristic masses around tens of $M_\odot$ (Turk, Abel & O’Shea 2009; Stacy, Greif & Bromm 2010; Greif et al. 2011b, 2012; Susa 2013). However, a recent paper by Hirano et al. (2014) studied 100 instances of Pop III protostar evolution with axisymmetric radiation hydrodynamics simulations that were initialized from a cosmological simulation. They found a wide range of possible stellar masses $M_* = 10$–1000 $M_\odot$, and under this scenario, our choice of a Pop III IMF would still be within the uncertainties gathered from such simulations.

6 CONCLUSIONS

We present the characteristic properties and abundances of dwarf galaxies at high redshift and their absolute contribution to cosmic reionization. To obtain our results, we use a cosmological radiation hydrodynamics simulation that considers Pop II and III star formation with a self-consistent transition with their radiative feedback modelled with the radiation transport module ENZO-MORAY. In a previous paper (W12), we showed that the star formation history and stellar population of the most massive dwarf galaxy in the simulation analysed here agreed with the local dwarf galaxy metallicity–luminosity relation. We have further analysed this simulation that captures the buildup of the first galaxies, starting with their Pop III progenitors, focusing on their global properties, LF, UV escape fraction, and role during reionization, and the highlights of our work are as follows.

(i) Low-luminosity galaxies with stellar masses up to $3 \times 10^4$ $M_\odot$, SFRs of $10^{-3} M_\odot$ yr$^{-1}$, and absolute UV magnitudes of $-12$ are able to form in metal cooling (MC) haloes ($T_{\mathrm{we}} \leq 10^6$ K). This usually occurs in one burst, which then suppresses any further star formation through stellar feedback, and star formation will recommence after sufficient gas has (re-)accreted into the potential well.

(ii) Gas fractions in the MC haloes have a large spread and are, on average, $\sim 5$–7 per cent, where $\sim 0.3$–3 per cent of this gas form stars. In addition to internal suppression, they are subsequently photosuppressed by an external radiation field.

(iii) The early dwarf galaxy LF flattens to $\sim 3$ mag$^{-1}$ Mpc$^{-3}$ at $M_{\mathrm{UV}} \gtrsim -12$. The galaxies in this plateau form in MC haloes usually with one star formation event that produces an initial magnitude around $M_{\mathrm{UV}} = -12$ and then increases as the stellar population ages.

(iv) The luminosity-weighted escape fraction decreases with halo mass with $f_{\mathrm{esc}} \simeq 0.5$ in haloes with $M \lesssim 2 \times 10^5$ $M_\odot$, $f_{\mathrm{esc}} \simeq 0.3$ in haloes with $2 \times 10^3 \lesssim M/M_\odot \lesssim 2 \times 10^6$, and $f_{\mathrm{esc}} \simeq 0.05$ in larger haloes. The escape fraction is highly time dependent and is correlated with the SFR with an average delay of $\sim 10$ Myr.

(v) The amount of ionizing photons per unit mass escaping from the halo, i.e. $f_{\mathrm{esc}} f_{\mathrm{gas}}$, shows little evolution with halo mass with a mean value of $10^{-3.6}$ over the mass range captured in our simulation.

(vi) Low-luminosity galaxies hosted in MC haloes propel the early epochs of reionization, providing 75 per cent of the instantaneous emissivity at $z = 14$ when our reionization model has an ionization fraction of 20 per cent. These faintest galaxies contribute nearly 30 per cent of the ionizing photon budget by $z = 6$.

(vii) Photosuppression of low-luminosity galaxies leads to a photon-starved reionization scenario by $z = 6$, agreeing with emissivities inferred from Ly$\alpha$ forest observations. By utilizing calibrated galaxy properties in our reionization model, we obtain an optical depth to Thomson scattering $\tau_e = 0.093$, agreeing with the latest WMAP and Planck results.

(viii) The luminosity-weighted escape fraction and host halo mass smoothly decline and increase, respectively, with time, and we have given functional fits (equations 17 and 18) to these trends for use in future studies.

We have shown that the faintest galaxies contribute a significant amount to the ionizing photon budget during cosmic reionization. Their consideration in reionization calculations is essential in order to adhere to observational constrains, such as $\tau_e$, the duration of reionization, a mostly ionized IGM by $z \sim 6$, and the ionization background at $z = 4$–6. We are currently following up this study with a larger data set with more massive galaxies (Xu et al. 2013) to further constrain galaxy scaling relations and galaxy observables during reionization, which is timely with the future launch of JWST and commissioning of 30-m class ground-based telescopes.

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