Abstract Magnetic experiments are powerful tools to study fundamental properties and to check the qualities of samples. Temperature, stress, and impurities of materials can all affect magnetic properties and play an important role in the utilization of these materials for engineering applications. The estimation and analysis of the spontaneous magnetization can reveal ferromagnetic particles as impurities in samples. The shape of the temperature dependence of magnetization is indicative of the origin of the magnetic properties. However, it is necessary to correlate the $\chi_m(T)$ curves and isothermal $M(H)$ plots to achieve a complete analysis of the electronic properties of the materials. Highlights of magnetic properties of lithium intercalation compounds are briefly described. Intrinsic and extrinsic properties are considered as useful parameters to determine the purity of electrode materials for rechargeable Li-ion batteries.

Keywords Li-ion batteries · Intercalation compounds · Magnetic properties · Clustering

Introduction

Magnetism continues to be an important subject, both to provide insights into the understanding of condensed matter and cooperative phenomena and for the development of technologically important materials and devices. Materials may be classified into five categories by their responses to externally applied magnetic fields, i.e., dia-, para-, ferro-, ferr-, and antiferromagnetic substances. The study of magnetic properties in the solid state implies an examination of the interaction between the electrons associated with the metal ions, which are substance-specific. Consequently, these magnetic properties differ greatly in strength. Diamagnetism is a property of all materials and opposes applied magnetic fields, but it is a very weak phenomenon. Paramagnetism, when present in semiconductors, can be stronger than diamagnetism and produces magnetization in the direction of the applied field, and proportional to the applied field. Ferromagnetic and ferrimagnetic effects are very large: They produce magnetizations sometimes orders of magnitude larger than the applied field and, as such, are much larger than either diamagnetic or paramagnetic effects.

Magnetic measurements can be extended to study magnetic structure and electronic properties of materials used in lithium power sources, i.e., the so-called lithium intercalation compounds (LiICs). Because Li ions are nonmagnetic (diamagnetic), they indirectly affect magnetic properties through influence on the cation valence of the 3d iron-transition element. Magnetic properties are determined by the structure of sublattice in the oxide framework, the nature of the metal ions, and the electronic states. In this context, magnetic properties are of particular interest because they are found to be a powerful tool to characterize materials, in particular, when impurities and nanoparticles cannot be detected by classical analysis, i.e., X-ray diffraction (XRD), Fourier transform infrared (FTIR) spectroscopy, etc. Magnetism is therefore indirectly important to the electrochemical properties of materials as well.

Magnetic measurements are also tools used to check the quality of samples. The estimation and analysis of the spontaneous magnetization can reveal the existence of ferromagnetic (ferrimagnetic) particles in samples. The shape of the temperature dependence of magnetization $M(H)$ is indicative of the origin of the magnetic properties. However, it is necessary to correlate the magnetic susceptibility $\chi_m(T)$ curves and isothermal $M(H)$ plots for a
complete analysis of the electronic properties of materials [1].

One goal of the work carried out in our laboratory is the understanding of the local structure in LiICs using resonance spectroscopy, i.e., Raman scattering, Fourier transform infrared, electron spin resonance, and magnetic measurements. This paper presents the magnetic properties of some LiICs to correlate the structural and electronic properties of oxides used as positive electrode materials in rechargeable lithium-ion batteries. Here, we consider typical materials such as compounds of the $\alpha$-NaFeO$_2$-type structure, i.e., LiNiO$_2$ and LiFeO$_2$; Li–Mn–O frameworks with the spinel structure, i.e., LiMn$_2$O$_4$ and LiCoMnO$_4$; and the phospho-olivine lattices, i.e., LiFePO$_4$, LiMnPPO$_4$, and LiNiPO$_4$. The characterization of the magnetic nanoparticles incorporated in these frameworks is deduced from the magnetic susceptibility and magnetization measurements.

**Experimental procedure**

Nowadays, most of the magnetic properties are studied by various techniques such as neutron diffractometry, magnetometry, NMR, and electron spin resonance. The two resonance spectroscopies are also useful tools for characterizing the local structure in materials.

The microscopic magnetic structure of materials is most often studied by using neutron scattering techniques, and experiments are performed to measure the structure and excitation for all classes of magnetic materials. More recently, synchrotron sources have been used to study the magnetic scattering. The range of wavelength and energy possessed by thermal moderated neutrons allows us to study not only the nuclear long-range, static nature of solids, but also the dynamics (phonons). Similarly, the neutron’s magnetic moment ($S=1/2$) can be used as a probe to study the magnetism in solids, allowing unparalleled scrutiny of both the magnetic structures (short- and long-range) and the excitations (magnons) of magnetic materials. Neutron scattering techniques are presently considered as the most powerful probe of magnetic materials. When a material has ferromagnetic ordering, the magnetic lattice is the same as the atom lattice, and no new “Bragg reflections” are created (the intensities of existing Bragg reflections change). For an antiferromagnetic state, however, the magnetic lattice is not the same as the atom lattice, and new, purely magnetic Bragg reflections occur. From the pattern of the magnetic Bragg reflections, the details of the antiferromagnetic ordering structure can be deduced, in the same way that crystal structures are solved from the pattern of the (nonmagnetic) Bragg peaks in XRD and (nuclear) neutron diffraction. Neutron diffraction patterns are currently analyzed using the Rietveld fitting procedure [2].

The use of superconducting quantum interference devices (SQUID) in ultra-sensitive magnetic measurement systems may nowadays be considered as a standard technique, to the extent that several companies offer reliable and automated commercial SQUID magnetometers. The SQUID consists of two superconductors separated by thin insulating layers to form two parallel Josephson junctions. The device uses a liquid-helium-cooled amplifier to measure the magnetic moment in the range from $10^{-7}$ to 300 emu. The field range is from −5.5 to +5.5 T [3].

Data on the temperature dependence of susceptibility are currently recorded on heating the sample using two modes to determine the magnetic behavior: zero-field cooling (ZFC) and field-cooling (FC). The procedure is based on performing two consecutive magnetization measurements: In ZFC, the sample is first cooled down in the absence of a magnetic field and then measured in an applied magnetic field at increasing temperature, FC is performed in a similar magnetic field at decreasing temperature. The results obtained in this way can exhibit a strong dependence of magnetization. The temperature range in which a magnetic hysteresis appears and the temperature at which a magnetic ordering can be detected should be emphasized.

**Magnetic properties of solid-state materials**

This section summarizes the general trends of magnetic properties for solid-state materials. In electrical engineering, the magnetic susceptibility is the degree of magneti-
zation of a material, $M$ is the magnetic dipole moment per unit volume in response to a magnetic field $H$, as

$$
\chi_m = \frac{\partial M}{\partial H}.
$$

If $\chi_m$ is positive, the material is called paramagnetic and the magnetic field is strengthened by the presence of the material. If $\chi_m$ is negative, then the material is diamagnetic and the magnetic field is weakened in the presence of the material. Figure 1 displays the temperature dependence of the magnetic susceptibility of paramagnetic, ferromagnetic, and antiferromagnetic solids [4].

Paramagnetic materials attract and repel like normal magnets when subjected to a magnetic field. For thermal equilibrium, the magnetization of paramagnets is treated using the Brillouin formalism. Under relatively low magnetic field saturation when the majority of atomic dipoles are not aligned with the field, paramagnetic materials exhibit magnetization according to the well-known Curie–Weiss law, which treats the interaction between spins and molecular field

$$
\chi_m = \frac{C_p}{T + \theta_p},
$$

where $C_p$ is the Curie constant. The Weiss constant, $\theta_p$, typically accounts for magnetic ordering of the electronic moments below the Curie or Néel temperature for uncorrelated spins (in salts, for instance) $\theta_p=0$ (see Fig. 1). For a paramagnet having an effective moment $\mu_{\text{eff}}$, the Curie constant is written as

$$
C_p = \frac{N_A p_{\text{eff}}^2 \mu_B^2}{3k_B},
$$

where $N_A$ is the molar concentration of ions and $\mu_B$ the Bohr magneton ($\mu_B=9.274 \times 10^{-24}$ J/T). The effective momentum number $p_{\text{eff}}$ is defined as

$$
p_{\text{exp}} = 2[S(S+1)]^{1/2},
$$

where $S$ refers to the electronic spin quantum number. Equation (4) is used in the case of the “quenching” of the orbital angular momentum ($L=0$ and $J=S$), which occurs frequently for transition-metal ions from the iron group. Table 1 shows the theoretical magneton numbers for iron group ions. Paramagnetic ions with electronic spin, $S$ (e.g., $S=3/2$ for $d^3$ ions Mn$^{4+}$ and Cr$^{4+}$), are associated with magnetic moments, $\mu_{\text{eff}}=\frac{gS\mu_B}{2}$, that align in the presence of static magnetic field $H_0$.

When the Curie constant is determined experimentally by fitting the linear $\chi_m(T)$ curve in the paramagnetic domain, one can estimate the experimental value for $p_{\text{eff}}$ and then know the electronic configuration of the magnetic ion (in the quenched configuration) using the following equation:

$$
p_{\text{eff}} = \left( \frac{3k_B C_p}{N_A \mu_B^2} \right)^{1/2} = 2.84 \sqrt{C_p}.
$$

An important class of magnetic materials is that of ferromagnets: iron, nickel, cobalt, and manganese. A ferromagnetic substance possesses a spontaneous magnetic moment even in the absence of an applied magnetic field.

### Table 1: Electron configurations and net spins for transition element cations and effective magneton numbers for iron group ions [5]

| Ion   | Configuration | Basic level | Free cation | Cubic field |
|-------|---------------|-------------|-------------|-------------|
|       |               |             | $S$ | $p_{\text{eff}}$ | $S$ | $p_{\text{eff}}$ |
| Mn$^{4+}$, Cr$^{3+}$ | 3$d^3$ | $^4$F$_{3/2}$ | 3/2 | 3.87 | 3/2 | 3.87 |
| Mn$^{3+}$, Cr$^{4+}$ | 3$d^4$ | $^3$D$_0$ | 2 | 4.90 | 1 | 2.83 |
| Fe$^{3+}$, Mn$^{2+}$ | 3$d^5$ | $^6$S$_{3/2}$ | 5/2 | 5.92 | 1/2 | 1.73 |
| Fe$^{2+}$, Co$^{3+}$ | 3$d^6$ | $^3$D$_4$ | 2 | 4.90 | 0 | 0 |
| Co$^{2+}$, Ni$^{3+}$ | 3$d^7$ | $^4$F$_{0/2}$ | 3/2 | 3.87 | 1/2 | 1.73 |
| Ni$^{2+}$ | 3$d^8$ | $^3$F$_4$ | 1 | 2.83 | 1 | 2.83 |
| Cu$^{2+}$ | 3$d^9$ | $^2$D$_{5/2}$ | 1/2 | 1.73 | 1/2 | 1.73 |

The free ions and cations in strong cubic fields are considered

![Graph](image-url)
The saturation magnetization $M_S$ is defined as the spontaneous magnetic moment per unit volume. The Curie point $T_C$ is the temperature above which the spontaneous moment vanishes. For iron, $T_C=1,043$ K [4].

The antiferromagnetic state is characterized by an ordered, antiparallel arrangement of electron spins. The simplest situation in antiferromagnetism arises when the lattice of paramagnetic ions can be divided into two interpenetrating sublattices. We recognize antiferromagnetism by a well-defined kink in the curve of the magnetic susceptibility vs temperature. This kink determines the Néel temperature, $T_N$. Antiferromagnets are also characterized by a negative value of the Curie temperature. Figure 1 summarizes the temperature dependence of the magnetic susceptibility for paramagnetic, ferromagnetic, and antiferromagnetic solids.

The paramagnetic temperature $\theta_p$ (also called the Weiss constant) is defined as the intercept of the temperature-axis of the high-temperature asymptote to the $\chi_m^{-1}(T)$ curve. Depending on the type of antiferromagnetic interactions, $\theta_p$ could be positive or negative. It should be emphasized that $\theta_p$ is different than the Néel temperature, $T_N$, which is the temperature at which an antiferromagnetic material becomes paramagnetic—that is, the thermal energy becomes large enough to upset the magnetic ordering within the material. $T_N$ corresponds to the cusp in the $\chi_m^{-1}(T)$ curve.

In metals, the conduction electrons are not spatially localized like electrons in partially filled ionic shells. Thus, the magnetic susceptibility of metals follows the Pauli-type paramagnetism, which is essentially independent on temperature [4]. In contrast, the magnetic susceptibility of localized electrons closely follows inverse temperature dependence due to the thermal agitation of spin moments. The magnetic molar susceptibility of localized moments will exhibit Curie–Weiss behaviors in the absence of strong ferromagnetic, ferrimagnetic, or antiferromagnetic couplings.

Many battery-grade materials are paramagnetic in the discharged or charged state. For example, the positive electrode material LiMn$_2$O$_4$ is a mixed-valence compound containing Mn$^{3+}$ ($d^4$) and Mn$^{4+}$ ($d^3$) ions. Although the low-spin ($d^5$) Co$^{3+}$ ions (nominally diamagnetic) in LiCoO$_2$ have paired d-electrons in the fully discharged state, Li$_{1-x}$CoO$_2$ contains Co$^{4+}$ ($d^3$) ions when charged. LiNiO$_2$ contains the paramagnetic $S=1/2$ ions Ni$^{3+}$ ($d^7$) in the discharged state.

### Magnetic properties of layered oxides

A wide variety of LiICs have been studied which include layered compounds based on the $\alpha$-NaFeO$_2$-type structure (e.g., LiCoO$_2$, LiNiO$_2$, LiNi$_{0.5}$Mn$_{0.5}$O$_2$). The structure-magnetic relationships of sodium and lithium ferrites have been investigated to evaluate detectable ferromagnetic impurities [6, 7]. The $\alpha$-NaFeO$_2$-type structure is built by alternating layers of trigonally distorted FeO$_6$ and NaO$_6$.
octahedra sharing edges. Many LiMO$_2$ (M=Ni, Co, Fe, and Cr) compounds have this typical structure which is suitable for very efficient electrochemical lithium extraction–insertion process. The unit cell is rhombohedral ($R \bar{3}m$ space group). The transition-metal ions M are located in octahedral 3$a$ (000) sites, and oxygen anions are in a cubic close-packing, occupying the 6$c$ (00z, 00z) sites. Li cations reside at Wyckoff 3$b$ (001/2) sites. The transition metal and lithium ions are occupying the alternating (111) planes.

$\alpha$-NaFeO$_2$

Samples of $\alpha$-NaFeO$_2$ prepared by hydrothermal treatment of a mixture of $\alpha$-FeOOH and concentrated NaOH aqueous solution appear as simple antiferromagnets below the Néel temperature $T_N=11$ K. Therefore, they do not include any ferromagnetic clusters such as Fe$_3$O$_4$ or $\gamma$-Fe$_2$O$_3$ particles. The temperature dependence of the molar magnetic susceptibility is shown in Fig. 2.

Fitting with the Curie–Weiss law, one obtains $C_p=4.17$ emu K/mol and $\theta_p=-10$ K. The negative $\theta_p$ value suggests that antiferromagnetic interactions are present in $\alpha$-NaFeO$_2$. Using Eq. (2), the effective magnetic moment, $\mu_{\text{eff}}$, is calculated to be 5.8 $\mu_B$, which is very close to a spin-only value of high-spin Fe$^{3+}$ ($5.92$ $\mu_B$).

The effective magnetic moment of LiFeO$_2$ is affected markedly by the contribution of ferromagnetic impurities, easily saturated at the magnetic fields used in the experiments. Two anomalies have been revealed at 40–50 and 90–280 K. The presence of a ferromagnetic impurity such as LiFe$_5$O$_8$ spinel gives a relatively high $\mu_{\text{eff}}$ value. The variation of the Néel temperature for various LiFeO$_2$ polymorphs is related to the degree of tetragonal distortion [8].

Fig. 5 Temperature of the ZFC and FC molar magnetic susceptibility measured under a field $H=50$ Oe of LiNi$_{1-y}$Co$_y$O$_2$ samples for $a_y=0.2$ and $b_y=0.3$. A strong deviation from the paramagnetic behavior is observed at low-temperatures for the $y=0.2$ sample

Fig. 6 ZFC magnetization vs applied magnetic field at $T=5$, 50, 100, and 300 K for LiNi$_{0.8}$Co$_{0.2}$O$_2$

Fig. 7 Size of the ferromagnetic clusters in LiNi$_{1-y}$Co$_y$O$_2$ samples
LiNiO₂

The difficulty of obtaining stoichiometric LiNiO₂ free from the presence of excess Ni ions randomly distributed at predominantly Li sites (3b Wyckoff position) is known. The magnetic properties are extremely sensitive to the Ni²⁺ ion distribution and should be useful to evaluate the stoichiometry deviation in Li₁₋ₓNiₓO₂. However, the confusion of magnetic properties lies in the quality of the sample. Hirakawa et al. suggested an S = 1/2 Ising-type antiferromagnetic triangular lattice in the crystal [9]. Other possibilities, such as ferri-magnetism [10], ferromagnetism [11], a new type of spin-frozen states [12], and spin glass [13–16], have been evoked.

Figure 3a shows the temperature dependence of the magnetic susceptibility of Li₀.⁹⁹Ni₁.⁰₁O₂. The insert displays the ZFC and FC low-temperature region. After ZFC, a cusp-like peak is observed at 8 K corresponding to the Néel temperature. On the other hand, the FC susceptibility shows little temperature dependence below Tₙ. Such behavior is that of a typical spin glass. The reciprocal susceptibility (Fig. 3b) follows the Curie–Weiss law above 100 K. The parameters obtained by least-square fitting [Eq. (2)] are \( C_p = 0.004 \) emu K/g and \( \theta_p = 30 \) K. The effective Bohr magneton number is \( p_{\text{eff}} = 1.77 \). This value is close to that of Ni³⁺ ion at low-spin state \( (S = 1/2, \ p = 2(S(S+1))^{1/2} = 1.73) \). The small deviation of the experimental \( p_{\text{eff}} \) is due to the presence of Ni²⁺ ions \( (S = 1, \ p = 2.83) \) at the 3b sites.

Considering that the total susceptibility of a given material is the sum the susceptibility of the various magnetic cations present in the lattice, the effective momentum number \( p_{\text{eff}} \) of Li₀.⁹⁹Ni₁.⁰₁O₂ is defined as

\[
p_{\text{eff}} = \left[ (1 - z)p_{\text{eff}}^2(\text{Ni}^{3+}) + zp_{\text{eff}}^2(\text{Ni}^{2+}) \right]^{1/2},
\]

As magnetic measurements are extremely sensitive to the Ni distribution, Eq. (6) is used to evaluate the stoichiometry deviation in Li₁₋ₐNi₁₊ₐO₂. From Fig. 3, one determines the quantity \( z = 0.01 \).

Figure 4 shows the applied magnetic field dependence on the magnetization curves \( M(H) \) as a function of the stoichiometric deviation, \( z \), in Li₁₋ₐNi₁₊ₐO₂. The samples were subjected to ZFC down to 4 K and a magnetic field was applied. These data, recorded at 40 K (paramagnetic phase), show clearly the systematic dependence of the effect of stoichiometric deviation on the magnetic behavior. The magnetization can be divided into an extrinsic component of ferromagnetic clusters which saturate easily under the application of a magnetic field of few hundred Gauss, plus the intrinsic part which remains linear in \( H \) up to the largest field investigated. Using the superparamag-

Fig. 8 Inverse ZFC and FC magnetic susceptibility for \( \lambda \)-Li₀.₀⁸Mn₂O₄ as a function of temperature in a field of 0.1 T.

Fig. 9 The reciprocal magnetic susceptibility of LiMn₂O₄ sample synthesis by succinic-assisted sol-gel method.
Because isostructural LiCoO$_2$—LiNiO$_2$ solid solutions display better electrochemical cyclability than parent oxide end-members, it is now generally recognized that LiNi$_{0.8}$Co$_{0.2}$O$_2$ is a potential next-generation positive electrode material to replace LiCoO$_2$. LiNi$_{1-y}$Co$_y$O$_2$ compounds with 0$\leq$y$\leq$1 were prepared as polycrystalline nanomaterials (d$\approx$200 nm) following a low-temperature sol-gel method [17]. XRD studies indicate that these materials are single phase for 0.2$\leq$y$\leq$1.0 with an ordered distribution of Li and Ni/Co in the layered structure. Nevertheless, as this technique provides only averaged structural information, it is still possible that, locally, there are some defects, among them disorder, that could affect the electrochemical behaviors of these materials. In fact, through FTIR spectroscopy, we observe for the Li–O band a slight deviation from a linear behavior for high nickel content (y$\leq$0.2), which is attributed to the presence of Ni cations in the octahedral interstices of the predominantly lithium layers (cation mixing). In addition, by means of magnetic measurements, $\chi_m$(T) and M(H), we detect in all the samples a ferrimagnetic signal, which gets smaller and smaller as the Co content increases, but indeed reveals the presence of some Ni$^{2+}$ ions occupying Li$^+$ sites that would lead to the formation of small ferromagnetic islands. From those magnetic measurements, we have estimated the size of nanometric magnetic inhomogeneities.

Figure 5a and b show the temperature dependence of the magnetic moment of LiNi$_{1-y}$Co$_y$O$_2$ for y=0.2 and y=0.3, respectively. The first general observation is that the samples with high Ni content (y$\leq$0.2) show ferrimagnetic behavior with a value of $T_c$, which quickly decreases from $T_c$(y=0)$\approx$215 K to $T_c$(y=0.2)$\approx$65 K as y increases, as seen in the $\chi_m$(T) and M(H) curves (Fig. 6). Taking into account that perfectly stoichiometric LiNiO$_2$ is considered to be a frustrated antiferromagnetic compound [18], this ferrimagnetic response would be indicative of the existence of Ni$^{3+}$ ions occupying Li$^+$ places [18, 19]. These interslab ions would lead to a ferromagnetic ordering of the Ni ions in two adjacent (Ni$_{1-y}$Co$_y$O$_2$)$_n$ slabs and to the formation of small ferromagnetic islands in their surroundings with the concomitant apparent ferrimagnetic behavior.

In the samples with intermediate substitutions (0.2$<y$$\leq$0.4), the magnetic features are different. Partial substitution of Ni$^{3+}$ by Co$^{3+}$ suppresses the ferrimagnetic response, reflecting that the addition of Co$^{3+}$ inhibits the presence of the interlayer Ni$^{2+}$ ions, and therefore favors a better lamellar structure. The positive Curie–Weiss constant calculated for 100$<T<300$ K ($\theta_p$$\approx$+30 K) shows that the Ni–O–Ni nearest neighbor interactions are still present at intermediate substitution levels. Apart from these general trends, magnetic measurements can also provide an approximation to the size of these magnetic islands. In this context, a blocking temperature, which decreases as
the Co content increases, is observed in all the ZFC- and FC-type curves for \( \chi_m(T) \). In the high-field region, at this temperature, it is possible to obtain the magnetic anisotropy, \( K \), from the magnetization measurements vs the magnetic field. To do so, we have to take into account that the magnetization approach to saturation can be fitted to the expression \[ M(H) = M_S \left( 1 - \frac{a}{H} - \frac{b}{H^2} \right) + cH, \] (9) where \( M_S \) is the saturation magnetization and \( a, b, \) and \( c \) are suitable constants. The second term, \( cH \), is the low-field contribution, which is negligible near the saturation. Two examples of these fits for the LiNi\(_{1-y}\)Co\(_y\)O\(_2\) samples with \( y = 0.2 \) and 0.4 can be seen in Fig. 7a,b, and that the \( b \) constant is related to the magnetic anisotropy, \( K \), by the expression \[ b = \beta \frac{K^2}{M_S^2}, \] (10) where \( \beta \) is a constant that depends on the type of material.

Assuming a typical value for the \( \beta \) constant (i.e., \( \beta = 0.0762 \) [21]), we can deduce the magnetic anisotropy constant from first magnetization curves from

\[ K = \left( \frac{bM_S^2}{0.0762} \right)^{1/2}. \] (11)

Following this procedure, we find that the magnetic anisotropy value, which is \( 6.5 \times 10^6 \) erg/cm\(^3\) for the LiNiO\(_2\) sample at 200 K, increases upon cobalt doping. Interestingly enough, these values are related to the volume of the magnetic clusters that lead to the blocking temperature in the \( \chi_m(T) \) ZFC- and FC-type curves. In this context, we can assume [1]

\[ KV = 25 k_B T_B, \] (12)

where \( V \) is the volume of the magnetic clusters, \( k_B \) is the Boltzmann’s constant, and \( T_B \) is the blocking temperature of each particular sample.

Now, supposing that these magnetic clusters are spherical, we obtain that they would have a mean radii of \( R = 3.5 \) nm in the case of the LiNiO\(_2\) sample, and that their size decreases upon Co-doping, becoming \( R = 1.2 \) nm in the sample with \( y = 0.2 \), and being further reduced to 0.5 nm in the samples with \( y = 0.3 \) and 0.4, as shown in Fig. 7.

**Magnetic properties of spinels**

The spinel material LiMn\(_2\)O\(_4\) can be cycled at ca. 4 V vs Li\(^+\)/Li from LiMn\(_2\)O\(_4\) to \( \lambda \)-MnO\(_2\) with manganese ions
LiFePO₄ samples synthesized by different sol-gel methods

The inverse of the magnetic susceptibility

Figure 14 The inverse of the magnetic susceptibility $\chi_m(T)$ of LiFePO₄ samples synthesized by different sol-gel methods

remaining the spinel host lattice throughout. LiMn₂O₄ spinel has shown interesting magnetic properties [22–27]. From the point of view of magnetic interactions, both direct ($\text{Mn}^{3+}/\text{Mn}^{4+}$) and superexchange ($90^\circ \text{Mn}^{3+}/\text{Mn}^{4+}$–$\text{O}^2$–$\text{Mn}^{3+}/\text{Mn}^{4+}$) interactions are conceivable between the nearest Mn neighbors. According to Goodenough, only $\text{Mn}^{4+}$–$\text{O}^2$–$\text{Mn}^{4+}$ interaction is in ferromagnetic coupling, while all other interactions are in antiferromagnetic coupling [28].

$\lambda$-Li$_{0.08}$MnO$_2$

Figure 8 shows the inverse magnetic susceptibility obtained after the lithium extraction from LiMn$_2$O$_4$. Over the temperature range 100–300 K, assuming that only the spin part of the Mn ions contributes to paramagnetic moment, the fit of the Curie–Weiss law is obtained with the following values: $\theta_p$=−75 K and $C_p$=3.29 emu K/mol. The $\theta_p$ value is negative, consistent with the apparent antiferromagnetic ordering below $T_N$=30 K. From the Curie constant, the effective moment is determined to be $\mu_{\text{eff}}=3.70\mu_B$, which is a value smaller than the theoretical spin-only value of $3.87\mu_B$ for $\text{Mn}^{3+}$ ion. An increase in the nominal manganese oxidation state from +3.5 to +4 should result in a greater covalence state due to the removal of $\sigma$ antibonding $e_g$ electrons associated with the manganese 3$d$ state. So, $\lambda$-MnO$_2$ has a greater covalency in the Li–O–$\text{Mn}^{3+}$ bond than in the Li–O–$\text{Mn}^{3.5+}$ bond.

The abrupt increase of magnetization (insert of Fig. 8) is noticeable with decreasing temperature below 30 K, indicating the presence of a ferromagnetic component. The origin of this ferromagnet could be a small amount of impurity phases, such as ferromagnetic Mn$_3$O$_4$, which is probably produced during the lithium extraction from LiMn$_2$O$_4$. However, the observation of spin-glass behavior at temperatures below the paramagnetic regime in the cubic phases LiMn$_2$O$_4$ and $\lambda$-Li$_{0.07}$MnO$_2$ has been reported by Jang et al. [24]. The existence of frozen spins is consistent with the presence of a significant fraction of spins disordered well below the Néel temperature. The value of the ratio $f=\theta_p/T_N$=2.5 is indicative of a frustrated antiferromagnet. The geometric frustration inherent in the Mn sublattice, which is comprised of a three-dimensional array of a corner-sharing tetrahedral, has been discussed by Greedan et al. [26].

LiMn$_2$O$_4$

Figure 9 shows the reciprocal magnetic susceptibility of a LiMn$_2$O$_4$ sample synthesized by wet-chemical technique, i.e., succinic-assisted sol-gel method [29]. In the temperature range 2–300 K, the ZFC and FC curves present complex behaviors including a Curie–Weiss law above 140 K. The extracted Curie–Weiss parameters are $\theta_p$=−260 K and $C_p$=4.85 emu K/mol. The negative Weiss constant indicates that antiferromagnetic interactions are dominant over ferromagnetic superexchange interactions in the paramagnetic temperature regime. These are the exchange interaction components across a shared octahedral-site edge in LiMn$_2$O$_4$ [30].

The measured effective magnetic moment is $\mu_{\text{eff}}=4.29\mu_B$. The value $p_{\text{eff}}=4.29$ is close to the theoretical spin-only value $p_{\text{eff}}=4.38$, assuming that only $\text{Mn}^{3+}$ and $\text{Mn}^{4+}$ moments are responsible to the paramagnetic behavior of $\chi_m(T)$, i.e., for $\text{Mn}^{3.5+}$ valence state ($p_{\text{eff}}=3.87$ and $C_p=1.87$ emu K/mol for $\text{Mn}^{3+}$; $p_{\text{eff}}=4.90$ and $C_p=3.0$ emu K/mol for $\text{Mn}^{4+}$). The magnetization curves display a clear splitting of the ZFC and FC data occurring below the paramagnetic temperature regime. A sharp maximum appears at 20 K in the ZFC magnetization. Jang et al. have reported a spin-glass-like behavior indicating the presence of frozen spins in cubic phases $\lambda$-MnO$_2$ and LiMn$_2$O$_4$ [31]. The randomness and frustration necessary for spin-glass-like behavior are explained by the octahedral antiferromagnetic network in the [Mn$_2$]O$_4$ sublattice spinel structure, combined with some magnetic disorder. The disorder due to the presence of a valence distribution in the Mn ions is provoked by competing ferro- and antiferromagnetic exchange interactions. This is believed to be responsible for the complex magnetic structure. Frozen spin was also observed in a neutron diffraction study by Oohara et al. [32]. Magnetic susceptibility measurements

![Fig. 15](image)
were also made on oxygen-deficient spinel LiMn$_2$O$_4$–$\delta$ ($\delta=0–0.1$) [33].

LiMn$_2$Co$_y$O$_4$

Various substitutions of manganese by different transition-metal cations have been investigated to improve their electrochemical properties [29]. The Jahn–Teller distortion associated with a large change in cell volume that occurs in the discharged state of LiMnO$_4$ is avoided with an increasing average oxidation state of manganese ions, $n_{\text{Mn}}>3.5^+$. On the basis of charge balance arguments, the substitution of a Mn ion for a dopant cation (e.g., Co, Cr, Ni, Al, Li, Zn, etc.) with charge $n^+$ will result in the oxidation of $2(3.5-n)$ Mn ions with average oxidation states of $3.5$ to Mn$^{4+}$.

Figure 10 shows the temperature dependence of the magnetic susceptibility of LiMn$_2$–$y$Co$_y$O$_4$ ($0\leq y\leq 1$) samples. In the low-temperature region, a drastic change in magnetization is observed upon substitution of Co for Mn. In particular, the strong anomaly at $T=30$ K disappears progressively with the introduction of Co$^{3+}$ ions in the spinel lattice. This is a consequence of the disappearance of the Mn$^{3+}$ ions in the [Mn$_2$]O$_4$ sublattice. For LiCoMnO$_4$, Mn$^{4+}$ is the only paramagnetic species. For the $y=1$ sample, the curve $\chi(T)$ can be represented by a straight line obeying the Curie–Weiss law $\chi_m^{-1}=(T-\theta_p)/C_p$ in the entire temperature range ($5–300$ K). The very large negative Weiss temperature $\theta_p=-260$ K for LiMnCoO$_4$ decreases to $\theta_p=-20$ K for LiMnCo$_2$O$_4$, indicating a weaker antiferromagnetic interaction. Hence, it appears that Mn$^{4+}$ ions in the [Mn$^{4+}$ Co$^{3+}$] environment have a stable configuration at low temperature. This observation suggests that the cobalt ions themselves must impart a larger electron spin density through the metal–oxygen–lithium bond in addition to the increasing presence of Mn$^{4+}$.

**Magnetic properties of Li-phosphates**

Recently, transition metal-based compounds containing compact tetrahedral polyanion structural units have been investigated intensively as potential positive electrode materials for lithium-ion batteries [34–36]. They are considered as stable, nontoxic, and friendly environmental materials. These compounds can exhibit various voltage-composition dependencies originating from their different structures.

| Compound       | $T_N$ (K) | $\theta_p$ (K) | $C_p$ (emu K/mol) | $\mu_{\text{eff}}$ |
|----------------|----------|----------------|-------------------|-------------------|
| LiMnPO$_4$     | 38       | $-68$          | 4.63              | 6.11              |
| LiNiPO$_4$     | 24       | $-65$          | 1.28              | 3.15              |
| LiCoPO$_4$     | 22       | $-77$          | 2.05              | 4.06              |
| LiFePO$_4$     | 52       | $-145$         | 4.18              | 5.77              |

**Phospho-olivine LiFePO$_4$**

The LiFePO$_4$ olivine structure belongs to the orthorhombic $Pnma$ space group. It consists of a distorted hexagonal close-packed framework containing Li and Fe in octahedral sites and P in tetrahedral sites. Each Li atom is connected by oxygen atoms to six FeO$_6$ units. The FeO$_6$ units are distorted, reducing the symmetry from $O_h$ to $C_s^2$. In $C_s$ symmetry, the metal d-orbitals split into $3A'$ orbitals at higher energy than the two remaining $A''$ orbitals, unlike $O_h$ symmetry, where two orbitals at higher energy are expected. The Fe magnetic ions are in the divalent Fe$^{2+}$ state, and occupy only the $M_2$ site, i.e., the center of the FeO$_6$ octahedron unit, while Li occupies only the $M_1$ site. As a consequence, Fe is distributed so as to form FeO$_6$ octahedra isolated from each other in TeO$_2$ layers perpendicular to the [001] hexagonal direction [37]. In addition, the lattice has a strong two-dimensional character because above a TeO$_2$ layer comes a second layer, at the vertical of the previous one, to build (100) layers of FeO$_6$ octahedra sharing corners, and mixed layers of LiO$_6$ octahedra and PO$_4$ octahedra.

Figure 11 displays the reciprocal ZFC and FC magnetic susceptibility of LiFePO$_4$ measured at $H=1$ T. LiFePO$_4$ undergoes an antiferromagnetic transition at $T_N=52$ K, with

![Fig. 16](image-url)
moments aligned along the [010] axis. The most outstanding property of the \( \chi_m^{-1}(T) \) curve for LiFePO\(_4\) lies in the fact that the deviation from the Curie–Weiss law remains small in the range 60–300 K. Values of Curie–Weiss constants deduced from the slope of the isothermal magnetization data (Fig. 11) are \( C_p = 4.18 \) emu K/mol and \( \theta_p = -145 \) K. These data are consistent with the magnetism of lithium iron phosphates where an antiferromagnetic ordering at low temperatures was reported [37]. The negative value of \( \theta_p \) is consistent with the antiferromagnetic coupling known for this compound. The value of the effective moment \( \mu_{\text{eff}} = 5.77 \mu_B \) is in agreement with what is expected for Fe(II) ions. The analysis of the exchange paths has been made by Mays [38].

Figure 12 displays the magnetization curves of LiFePO\(_4\) in the temperature range 4–300 K. Due to the existence of a ferromagnetic component, the magnetization is not a linear function of the magnetic field. The first consequence is an ambiguity in what is called magnetic susceptibility \( \chi_m \), because \( M/H \) is distinct from \( dM/dH \). Because all the magnetic measurements have been performed on a SQUID magnetometer (and not a Faraday balance), the quantity measured is the magnetization \( M \) in an applied magnetic field \( H \), so that we shall use the notation \( \chi_m = M/H \). The other consequence of the nonlinearity of the magnetization is that the data recorded in the “long-moment” made by the SQUID apparatus are not sufficient to get an understanding of the magnetic susceptibilities, and the full investigation of the magnetization as a function of the magnetic field at different temperatures is needed for this purpose (Fig. 13).

The inverse of the magnetic susceptibility \( \chi_m(T) \) of LiFePO\(_4\) samples synthesized by different sol-gel methods is reported as a function of temperature in Fig. 14. At contrast with prior works, these data give evidence of a ferromagnetic ordering at Curie temperature \( T_C \approx 216 \) K, while we expected the evidence of an antiferromagnetic ordering at 52 K. Below \( T_C \), the magnetic susceptibility is independent of temperature, and thus only depends on a demagnetization factor. Above \( T_C \), the Curie–Weiss law is approximately satisfied with a Curie–Weiss temperature close to \( T_C \). The effective Curie constant, however, is sample-dependent. In addition, the Curie–Weiss law is a mean-field law, and thus, valid only far from \( T_C \). This condition, even at room temperature, is not fulfilled, which precludes any quantitative analysis of the magnetic susceptibility curves in Fig. 14 in this framework. Due to the existence of a large ferromagnetic component, the magnetization is not a linear function of the magnetic field [39].

### LiMPO\(_4\) olivine-related compounds

Other olivine structures LiMPO\(_4\) include compounds with \( M = \text{Ni}, \text{Co}, \) and \( \text{Mn} \). The temperature dependence of the inverse magnetic susceptibility measured with a SQUID magnetometer is shown in Fig. 15. All compounds exhibit a Curie–Weiss-type dependence on temperature. The data are consistent with the magnetism of LiFePO\(_4\), where antiferromagnetic ordering appears at low temperatures. Linear fits provided the Weiss constants and the effective magnetic moments (Table 2), which can be compared to the theoretical spin-only values in Table 1. The reduced MO\(_6\) symmetric has a noticeable effect on the magnetic susceptibility of LiCoPO\(_4\). We note that Co\(^{2+}\) is expected to have three unpaired electrons (\( A' \)) in \( C_t \) symmetry, consistent with the experimental data, but only a single unpaired electron (\( e_g \)) in \( O_h \) symmetry [40].

The magnetic structures in the ordered phases are both collinear for olivines: in LiMnPO\(_4\) the magnetic moments are parallel to the \( a \)-axis, while in LiFePO\(_4\) and LiCoPO\(_4\), to the \( b \)-axis. In this case, the orbital angular momentum is not completely quenched, and spin-orbit coupling aligns spins along the \( b \)-axis. The distance between magnetic ions is one of the strongest factors affecting the magnetic exchange strength. This distance variation accounts well for the observed transition temperature: The highest \( T_N \) corresponds to the strongest exchange.

For the LiFePO\(_4\) phospho-olivine structure, the magnetic properties give evidence of nano-sized ferromagnetic particles, which can be either strongly magnetic (\( \gamma - \text{Fe}_2\text{O}_3 \) clusters) or weakly ferromagnetic (Fe\(_2\)P clusters), depending on the preparation process. The concentration of magnetic clusters also depends on the preparation process and varies from small concentrations (1.0×10\(^{-6} \) of \( \gamma - \text{Fe}_2\text{O}_3 \) per formula), in which case, noncollective behavior is observed, to large concentrations (1.9×10\(^{-4} \) of Fe\(_2\)P clusters per formula) where the dipolar interaction generates superferromagnetism. Ferromagnetic resonance experiments are also reported and are a probe of the \( \gamma - \text{Fe}_2\text{O}_3 \) nanoparticles. An overall understanding of the different properties is achieved within a model of superferromagnetism induced by interacting Fe\(_2\)P nanoparticles (Ait Salah et al., unpublished).

### Li\(_3\)M\(_2\)(PO\(_4\))\(_x\) compounds

Among the lithium metal polyphosphate family, the compounds described by formula Li\(_3\)M\(_2\)(PO\(_4\))\(_x\) (\( M = \text{Fe, V, Mo and } x = 3, 5, 6, \) respectively) crystallize with the Nasicon-like structure [41]. Plots of the magnetic susceptibility, as a function of temperature for Fe- and V-containing compounds, are shown in Fig. 16. The calculated Curie temperature value equals \( \theta = -46.7 \) K for Li\(_3\)Fe\(_2\)(PO\(_4\))\(_3\) and \( \theta = -0.1 \) K for Li\(_3\)V\(_2\)(PO\(_4\))\(_5\). The negative Curie temperature indicates an antiferromagnetic behavior of the studied materials at temperatures above their Néel point. For Li\(_3\)Fe\(_2\)(PO\(_4\))\(_3\), the magnetic moment \( \mu_{\text{eff}} = 5.90 \mu_B \) is comparable with the theoretical value of Fe\(^{3+}\) (5.92 \( \mu_B \)). For the Li\(_3\)V\(_2\)(PO\(_4\))\(_5\) sample, one obtains \( \mu_{\text{eff}} = 1.56 \mu_B \), while the theoretical value equals 1.55 \( \mu_B \) for \( V^{3+} \) and 1.63 \( \mu_B \) for \( V^{4+} \). Values of the magnetic moment for both studied materials are associated with the most occupied transition metal sites [Fe\(^{3+}\) for Li\(_3\)Fe\(_2\)(PO\(_4\))\(_3\) and V\(^{4+}\) for Li\(_3\)V\(_2\)(PO\(_4\))\(_5\), respectively]. For the Mo compounds, a different behavior is observed. This material behaves as a diamagnetic material (i.e., its susceptibility is
negative and temperature-independent) in the whole range of temperature.

Conclusion

For LiNi$_1-y$Co$_y$O$_2$ materials prepared by wet chemistry, the magnetic measurements of $\chi_m(T)$ and $M(H)$ have revealed the presence of small ferromagnetic islands arising from the fact that some Ni$_{2+}$ ions are occupying Li$^+$ places, which leads to a ferromagnetic ordering of the Ni ions in two adjacent (Ni,CoO$_2$)$_n$ slabs. The size of these clusters gets smaller and smaller as the Co content increases from $R_{(n=0)}=3.5$ nm to $R_{(n=0.4)}=0.5$ nm. Magnetic characterization of LiMn$_2$O$_4$ spinel materials shows a spin-glass behavior below the paramagnetic regime ($T_s<25$ K). The magnetic properties are determined by interactions between the Mn ions, which in turn depend on the Mn valence distribution in the [Mn$_2$O$_4$] framework. The short-range antiferromagnetic order is also investigated in the case of cobalt-substituted spinels, namely, LiMn$_{y}$Co$_{1-y}$O$_4$.

For LiFePO$_4$ phospho-olivine material, the magnetic properties give evidence of nano-sized ferromagnetic particles, which can be either strongly magnetic (γ-Fe$_2$O$_3$ clusters) or weakly ferromagnetic (Fe$_2$P clusters), depending on the preparation process. The concentration of magnetic clusters also depends on the preparation process and varies from small concentration ($1.0 \times 10^{-6}$ of γ-Fe$_2$O$_3$ per formula), in which case, noncollective behavior is observed, to large concentrations ($1.9 \times 10^{-4}$ of Fe$_2$P clusters per formula) where the dipolar interaction generates superferromagnetism. Ferromagnetic resonance experiments are also reported and are a probe of the γ-Fe$_2$O$_3$ nanoparticles. An overall understanding of the different properties is achieved within a model of superferromagnetism, which is induced by interacting Fe$_2$P nanoparticles. The magnetic structure of LiMPO$_4$ phospho-olivine lattices is just that which is predicted by the application of Anderson’s theory of superexchange to $M$–$O$–$P$–$O$–$M$ linkages.

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