When Humans Aren’t Optimal: Robots that Collaborate with Risk-Aware Humans

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Abstract

In order to collaborate safely and efficiently, robots need to anticipate how their human partners will behave. Some of today’s robots model humans as if they were also robots, and assume users are always optimal. Other robots account for human limitations, and relax this assumption so that the human is noisily rational. Both of these models make sense when the human receives deterministic rewards: i.e., gaining either $100 or $130 with certainty. But in real-world scenarios, rewards are rarely deterministic. Instead, we must make choices subject to risk and uncertainty—and in these settings, humans exhibit a cognitive bias towards suboptimal behavior. For example, when deciding between gaining $100 with certainty or $130 only 80% of the time, people tend to make the risk-averse choice—even though it leads to a lower expected gain! In this paper, we adopt a well-known Risk-Aware human model from behavioral economics called Cumulative Prospect Theory and enable robots to leverage this model during human-robot interaction (HRI). In our user studies, we offer supporting evidence that the Risk-Aware model more accurately predicts suboptimal human behavior. We find that this increased modeling accuracy results in safer and more efficient human-robot collaboration. Overall, we extend existing rational human models so that collaborative robots can anticipate and plan around suboptimal human behavior during HRI.

CCS Concepts

• Mathematics of computing → Probabilistic inference problems; • Computing methodologies → Cognitive robotics; Theory of mind.

Keywords
cognitive HRI; cumulative prospect theory; human prediction

1 Introduction

When robots collaborate with humans, they must anticipate how the human will behave for seamless and safe interaction. Consider a scenario where an autonomous car is waiting at an intersection (see top of Fig. 1). The autonomous car wants to make an unprotected left turn, but a human driven car is approaching in the oncoming lane. The human’s traffic light is yellow, and will soon turn red. Should the autonomous car predict that this human will stop—so that the autonomous car can safely turn left—or anticipate that the human will try and make the light—where turning left leads to a collision?

Previous robots anticipated that humans acted like robots, and made rational decisions to maximize their reward [1, 18, 25, 36, 44, 45]. However, assuming humans are always rational fails to account for the limited time, computational resources, and noise...
that affect human decision making, and so today’s robots anticipate that humans make noisily rational choices [13, 17, 32, 37, 47]. Under this model, the human is always most likely to choose the action leading to the highest reward, but the robot also recognizes that the human may behave suboptimally. This makes sense when humans are faced with deterministic rewards: e.g., the light will definitely turn red in 5 seconds. Here, the human knows whether or not they will make the light, and can accelerate or decelerate accordingly. But in real world settings, we usually do not have access to deterministic rewards. Instead, we need to deal with uncertainty and estimate risk in every scenario. Returning to our example, imagine that the human has a 95% chance of making the light if they accelerate: success saves some time during their commute, while failure could result in a ticket or even a collision. It is still rational for the human to decelerate; however, a risk-seeking user will attempt to make the light. How the robot models the human affects the safety and efficiency of this interaction: a Noisy Rational robot believes it should turn left, while a Risk-Aware robot realizes that the human is likely to run the light, and waits to prevent a collision.

When robots treat nearby humans as noisily rational, they miss out on how risk biases human decisions. Instead, we assert that people behave suboptimally when risk is involved.

Our approach is inspired by behavioral economics, where results indicate that users maintain a nonlinear transformation between actual and perceived rewards and probabilities [20, 42]. Here, the human over- or under-weights differences between rewards, resulting in a cognitive bias (a systematic error in judgment) that leads to risk-averse or risk-seeking behavior. We equip robots with this cognitive model, enabling them to anticipate risk-affected human behavior and better collaborate with humans in everyday scenarios (see Fig. 1).

Overall, we make the following contributions:

**Incorporating Risk in Robot Models of Humans.** We propose using Cumulative Prospect Theory as a Risk-Aware model. We formalize a theory-of-mind (ToM) where the robot models the human as reacting to their decisions or environmental conditions. We integrate Cumulative Prospect Theory into this formalism so that the robot can model suboptimal human actions under risk. In a simulated autonomous driving environment, our user studies demonstrate that the Risk-Aware robot more accurately predicts the human’s behavior than a Noisy Rational baseline.

**Determining when to Reason about Risk.** We identify the types of scenarios where reasoning about risk is important. Our results suggest that scenarios with close expected rewards is the most important in determining whether humans will act suboptimally.

**Safe and Efficient Collaboration when Humans face Uncertainty.** We develop planning algorithms so that robots can leverage our Risk-Aware human model to improve collaboration. In a collaborative cup stacking task, shown on the bottom in Fig. 1, the Risk-Aware robotic arm anticipated that participants would choose suboptimal but risk-averse actions, and planned trajectories to avoid interfering with the human’s motions. Users completed the task more efficiently with the Risk-Aware robot, and also subjectively preferred working with the Risk-Aware robot over the Noisy Rational baseline.

This work describes a computationally efficient and empirically supported way for robots to model suboptimal human behavior by extending the state-of-the-art to also account for risk. A summary of our paper, including videos of experiments, can be found here.

## 2 Related Work

Previous work has shown that robots that successfully predict humans’ behavior exhibit improved performance in many applications, such as assistive robotics [2, 14, 22, 23], motion planning [27, 48], collaborative games [26], and autonomous driving [3, 38, 39]. One reason behind this success is that human modeling equips robots with a theory of mind (ToM), or the ability to attribute a mind to oneself and others [34, 41]. Devin and Alami [11] showed ToM can improve performance in human-robot collaboration.

For this purpose, researchers have developed various human models. In robotics, the Noisy Rational choice model has remained extremely popular due to its simplicity. Several works in reward learning [5–7, 9, 32, 37], reinforcement learning [17], inverse reinforcement learning [8, 35, 47], inverse planning [4], and human-robot collaboration [33] employed the noisy rational model for human decision-making. Other works developed more complex human models and methods specifically for autonomous driving [18, 21, 38, 44]. Unfortunately, these models either assume humans are rational or do not handle situations with uncertainty and risk. There have been other human models that take a learning-based approach [30, 31, 43]. While this is an interesting direction, these methods are usually not very data efficient.

In cognitive science, psychology and behavioral economics, researchers have developed other decision-making models. For example, Ordonez and Benson III [28] investigated decision making under time constraints; Diederich [12] developed a model based on stochastic processes to model humans’ process of making a selection between two options, again under a time constraint. Ortega and Stocker [29] proposed a rationality model based on concepts from information theory and statistical mechanics to model time-constrained decision making. Mishra [24] studied decision making under risk from the perspectives of biology, psychology and economics. Halpern et al. [19] modeled the humans as a finite automata, and Simon [40] developed bounded rationality to incorporate suboptimalities and constraints. Evans et al. [16] investigated different biases humans can have in decision-making. Among all of these works, Cumulative Prospect Theory (CPT) [42] remains prominent as it successfully models suboptimal human decision making under risk. Later works studied how Cumulative Prospect Theory can be employed for time-constrained decision making [15, 46].

In this paper, we adopt Cumulative Prospect Theory as an example of a Risk-Aware model. We show that it not only leads to more accurate predictions of human actions, but also increases the performance of the robot and the human-robot team.

## 3 Formalism

We assume a setting where a human needs to select from a set of actions $\mathcal{A}_H$. Each action $a_H \in \mathcal{A}_H$ may have several possible consequences, where, without loss of generality, we denote the number of consequences as $K$. For a given human action $a_H$, we express the probabilities of each consequence and their corresponding rewards
as a set of pairs:

\[ C(a_H) = \left\{ \left( p^{(1)}_H, R^{(1)}_H(a_H) \right), \left( p^{(2)}_H, R^{(2)}_H(a_H) \right), \ldots, \left( p^{(K)}_H, R^{(K)}_H(a_H) \right) \right\} \]

We outline and compare two methods that use \( C(a_H) \) to model human actions: Noisy Rational and Cumulative Prospect Theory (CPT) \([42]\). CPT is a prominent model of human decision-making under risk \([15, 46]\) and we use it as an example of a Risk-Aware model. Finally, we describe how we can integrate them into a partially observable Markov decision process (POMDP) formulation of human-robot interaction.

**Noisy Rational Model.** According to the noisy rational model, humans are more likely to choose actions with the highest expected reward, and are less likely to choose suboptimal actions (i.e., they are optimal with some noise). The noise comes from constraints such as limited time or computational resources. For instance, in the autonomous driving example, Noisy Rational model would predict the human will most likely choose the optimal action and decelerate. Denoting the expected reward of the human for action \( a_H \) as

\[ R_H(a_H) = p^{(1)}_H R^{(1)}_H(a_H) + p^{(2)}_H R^{(2)}_H(a_H) + \ldots + p^{(K)}_H R^{(K)}_H(a_H), \]

the noisy rational model asserts

\[ P(a_H) = \frac{\exp \left( \theta \cdot R_H(a_H) \right)}{\sum_{a \in A_H} \exp \left( \theta \cdot R_H(a) \right)}, \quad (1) \]

where \( \theta \in [0, \infty) \) is a temperature parameter, commonly referred to as the *rationality coefficient*, which controls how noisy the human is. While larger \( \theta \) models the human as a better reward maximizer, setting \( \theta = 0 \) means the human chooses actions uniformly at random.

Hence, the Noisy Rational model is simply a linear transformation of the reward with the rationality coefficient \( \theta \geq 0 \), which makes the transformation monotonically non-decreasing. As the model does not transform the probability values, it becomes impossible to model suboptimal humans using this approach. The closest Noisy Rational model can get to modeling suboptimal humans is to assign a uniform probability to all actions.

**Risk-Aware Model.** We adopt Cumulative Prospect Theory (CPT) \([42]\) as an example of a Risk-Aware model. According to this model, humans are not simply Noisy Rational. They may, for example, be suboptimally risk-seeking or risk-averse. For instance, in the autonomous driving example, human drivers can be risk-seeking and try to make the yellow light even though they risk a costly collision. The Risk-Aware model captures suboptimal decision-making by transforming both the probabilities and the rewards. These transformations aim to represent what humans actually perceive. The reward transformation is a pairwise function:

\[ v(R) = \begin{cases} R^\alpha & \text{if } R \geq 0 \\ -\lambda (-R)^\beta & \text{if } R < 0 \end{cases} \]

The parameters \( \alpha, \beta \in [0, 1] \) represent how differences among rewards are perceived. For instance, when \( \alpha, \beta \in (0, 1) \), the model predicts that humans will perceive differences between large positive (or negative) rewards as relatively lower than the differences between smaller positive (resp. negative) rewards, even though the true differences are equal. \( \lambda \in [0, \infty) \) characterizes how much more (or less) important negative rewards are compared to positive rewards. When \( \lambda > 1 \), humans are modeled as loss-averse, assigning more importance to losses compared to gains. The reverse is true when \( \lambda \in [0, 1) \).

The Risk-Aware model also implements a transformation over the probabilities. The probabilities \( (p^{(1)}, p^{(2)}, \ldots) \) are divided into two groups based on whether their corresponding true rewards are positive or negative. The probability transformations corresponding to positive and negative rewards \( (w^+, w^-) \) are as follows:

\[ w^+(p) = \frac{p^\lambda}{(p^\gamma + (1 - p^\gamma)^\gamma)}, \quad w^-(p) = \frac{p^\delta}{(p^\beta + (1 - p^\beta)^\beta}, \]

where \( \gamma, \delta \in [0, 1) \).

Without loss of generality, we assume that each of the \( K \) rewards are ordered in decreasing order, i.e. \( R_H^{(i+1)}(a) \leq R_H^{(i)}(a) \) for all \( i \in \{1, 2, \ldots, K-1\} \) and \( a \in A_H \). Then, the probability transformation is as follows:

\[ \pi(C(a_H)) = \pi^+(C(a_H)), \quad \pi^+(C(a_H)) = \left( w^+(p^{(1)}), w^+(p^{(1)} + p^{(2)}) - w^+(p^{(1)}), \ldots \right) \]

\[ \pi^-(C(a_H)) = \left( \ldots, w^-((p^{(K)} + p^{(K-1)}) - w^-((p^{(K)}), w^-((p^{(K)})) \right) \]

Finally, we normalize probabilities so that \( \pi(C(a_H)) \) sums to 1:

\[ \pi_j(C(a_H)) = \frac{\pi_j(C(a_H))}{\sum_{i=1}^{K} \pi_i(C(a_H))}, \forall j \in \{1, 2, \ldots, K\} \]

When \( \gamma, \delta \in (0, 1) \), the probability transformations capture biases humans are reported to have \([42]\) by overweighting smaller probabilities and underweighting larger probabilities.

Based on these two transformations, we now extend the human decision making model with the Risk-Aware model:

\[ R_H^{\text{CPT}}(a_H) = \pi^+(C(a_H)) \cdot v(R_H^{(1)}(a_H)) + \ldots + \pi^+(C(a_H)) \cdot v(R_H^{(K)}(a_H)) \]

\[ P(a_H) = \frac{\exp \left( \theta \cdot R_H^{\text{CPT}}(a_H) \right)}{\sum_{a \in A_H} \exp \left( \theta \cdot R_H^{\text{CPT}}(a) \right)}, \quad (2) \]

In contrast to the Noisy Rational model, the Risk-Aware model’s expressiveness allows it to model both optimal and suboptimal human decisions by assigning larger likelihoods to those actions. **Formal Model of Interaction.** We model the world where both the human and the robot take actions as a POMDP, with a denote with a tuple \((S, O, O_H, A_{HT}, A_R, T_{HT}, T_{HR}, r_{HT}, r_{HR})\). \( S \) is the set of states; \( O \) is the set of observations; \( O: S \rightarrow O \) defines the shared observation mapping; \( A_H \) and \( A_R \) are the finite action sets for the human and the robot, respectively; \( T: S \times A_H \times A_R \times S \rightarrow [0, 1] \) is the transition distribution. \( T_{HT} \) and \( r_{HT} \) are the reward functions that depend on the state, the actions and the next state. In this POMDP, we assume the agents act simultaneously. Having a first-order ToM, the human tries to optimize her own cumulative reward given an action distribution for the robot, \( P(a_H|s) \). The human value function \( V_H(s) \) can then be defined using the following Bellman update:

\[ V_H(s) = \max_{a_H \in A_H} \mathbb{E}_{a_R | s} \left[ V_H(s') + \gamma V_H(s') \right] \]

We then use the fact that

\[ P(s, s', a_H | a_R, a_H) = P(s | a_R) \cdot P(a_R | s) \cdot P(s' | s, a_H, a_R) \]

to construct a set \( C(a_H) \) for the current observation \( o \) that consists of the pairs \((P(s, s', a_H | a_R, V_H(s')) \) for varying \( s, s' \), and \( a_R \).
When modeling the human as zeroth-order ToM, \( P(a_R \mid s) \) will simply be a uniform distribution.

Having constructed \( C(a_H) \), we can define the human’s utility function for different values of \( s \), and \( s' \). The utility functions for both Noisy Rational and Risk-Aware models are defined as follows:

**Noisy Rational:**

\[
R^o_H(o, a_H) = \sum_{s, s' \in S} \sum_{a_R \in A_R} P(s, s', a_R \mid o, a_H) \cdot V_H(s') .
\]

**Risk-Aware:**

\[
R^{\text{CPT}}_H(o, a_H) = \sum_{s, s' \in S} \sum_{a_R \in A_R} \pi_i(P(s, s', a_R \mid o, a_H)) \cdot v(V_H(s')) ,
\]

where the index \( i \) corresponds to the event that leads to \( s' \) from \( s \) with \( a_R, a_H \). An optimal human would always pick the action \( a_H \) that maximizes \( E_{s}[E_{a_R}[E_{s'}[V_H(s') \mid a_H, a_R]]] \). The robot can obtain \( P(a_H \mid o) \) using Eqn. (1), Eqn. (2) and use it to maximize its own cumulative reward.

**Summary.** We have outlined two ways in which we can model humans (Noisy Rational and Risk-Aware), and how we can formalize these models in a human-robot interaction setting. In the following section, we empirically analyze factors that allow the Risk-Aware robot to more accurately model human actions.

### 4 Autonomous Driving

In our first user study, we focus on the autonomous driving scenario from the bottom of Fig. 1. Here the autonomous car—which wants to make an unprotected left turn—needs to determine whether the human-driven car is going to try to make the light. We asked human drivers whether they would accelerate or stop in this scenario. Specifically, we adjusted the information and time available for the human driver to make their decision. We also varied the level of risk by changing the probability that the light would turn red. Based on the participant’s choices in each of these cases, we learned Noisy Rational and Risk-Aware human models. Our results demonstrate that autonomous cars that model humans as Risk-Aware are better able to explain and anticipate the behavior of human drivers, particularly when drivers make suboptimal choices.

**Experimental Setup.** We used the driving example shown in Fig. 1. Human drivers were told that they are returning a rental car, and are approaching a light that is currently yellow. If they run the red light, they have to pay a $500 ticket. But stopping at the light will prevent the human from returning their rental car on time, which also has an associated fine! Accordingly, the human drivers had to decide between accelerating (and potentially running the light) or stopping (and returning the rental car with a fine).

**Independent Variables.** We varied the amount of information and time that the human drivers had to make their decision. We also tested two different risk levels: one where accelerating was optimal, and one where stopping was optimal. Our parameters for information, time, and risk are provided in Table 1.

| Information       | Time         |
|-------------------|--------------|
| None: With some probability the light will turn red. | Timed: 8 s |
| Explicit: There is a 5% chance the light will turn red. | Not Timed: no limit |
| Implicit: Of the previous 380 cars that decided to accelerate, the light turned red for 19 cars. | Risk |

| Risk      | High: 95% | Low: 5% |
|-----------|-----------|---------|
| Time      | Timed:    | Not Timed: |
|           | 60%       | 77%     |
|           | 55%       | 57%     |

**Dependent Measures.** We aggregated the user responses into action distributions. These action distributions report the percentage of human drivers who chose to accelerate and stop under each treatment level. Next, we learned Noisy Rational and Risk-Aware models of human drivers for the autonomous car to leverage.

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1. To learn more about our study, please check out our autonomous driving survey link: https://standfordghb.qualtrics.com/jfe/form/SV_cUgxaZVeckb3ud
2. To learn the models, we used the Metropolis-Hastings algorithm [10] and obtained 30 independent samples of the model parameters.
Log KL Divergence

where the light frequently turns red (High), both models produce similar transformations. But when the light rarely turns red (Low), the

Figure 4: Model accuracy (lower is better). When the light often turns red (High), both models could anticipate the human’s behavior. But when the light rarely turns red (Low), only the Risk-Aware autonomous car correctly anticipated that the human would stop.

measure the accuracy of these models, we compared the Kullback-Leibler (KL) divergence between the true action distribution and the model’s predicted action distribution. We report the log KL divergence for both Noisy Rational and Risk-Aware models.

Hypothesis.

H1. Autonomous cars which use Risk-Aware models of human drivers will more accurately predict human action distributions than autonomous cars who treat humans as noisy rational agents.

Baseline. In order to confirm that our users were trying to make optimal choices, we also queried the human drivers for their preferred actions in settings where the expected rewards were far apart (e.g., where the expected reward for accelerating was much higher than the expected reward for stopping). In these baseline trials, users overwhelmingly chose the optimal action (93% of trials).

Results. The results from our autonomous driving user study are summarized in Figs. 2, 3, and 4. In each of the tested situations, most users elected to stop at the light (see Fig. 2). Although stopping at the light is the optimal action in the High risk case—where the light turns red 95% of the time—stopping was actually suboptimal in the Low risk case—where the light only turns red 5% of the time. Because humans chose optimal actions in some cases (High risk) and suboptimal actions in other situations (Low risk), the autonomous car interacting with these human drivers must be able to anticipate both optimal and suboptimal behavior.

In cases where the human was rational, autonomous cars learned similar Noisy Rational and Risk-Aware models (see Fig. 3). However, the Risk-Aware model was noticeably different in situations where the human was suboptimal. Here autonomous cars using our formalism learned that human drivers overestimated the likelihood that the light would turn red, and underestimated the reward of running the light. Viewed together, the Risk-Aware model suggests that human drivers were risk-averse when the light rarely turned red, and risk-neutral when the light frequently turned red.

Autonomous cars using our Risk-Averse model of human drivers were better able to predict how humans would behave (see Fig. 4). Across all treatment levels, Risk-Averse attained a log KL divergence of $-5.7 \pm 3.3$, while Noisy Rational only reached $-3.3 \pm 1.3$. This difference was statistically significant ($t(239) = -11.5, p < .001$). Breaking our results down by risk, in the High case both models were similarly accurate, and any differences were insignificant ($t(119) = .42, p = .67$). But in the Low case—where human drivers were suboptimal—the Risk-Averse model significantly outperformed the Noisy Rational baseline ($t(119) = -17.3, p < .001$).

Overall, the results from our autonomous driving user study support hypothesis H1. Autonomous cars leveraging a Risk-Averse model were able to understand and anticipate human drivers both in situations where the human is optimal or suboptimal, while the Noisy Rational model could not explain why the participants preferred to take a safer (but suboptimal) action.

Follow-up: Disentangling Risk and Suboptimal Decisions. After completing our user study, we performed a simulated experiment within the autonomous driving domain. Within this experiment, we fixed the probability that the light would turn red, and then varied the human driver’s action distribution. When fixing the probability, we used the High risk scenario where the optimal decision was to stop. The purpose of this follow-up experiment was to make sure that our model can also explain suboptimally aggressive drivers, and to ensure that our results are not tied to the Low risk scenario. Our simulated results are displayed in Fig. 5. As before, when the human driver chose the optimal action, both Noisy Rational and Risk-Aware models were equally accurate. But when
Within the autonomous driving user studies, we demonstrated that Noisy Rational, which cups its human partner would pick up. where the human and robot collaborate to stack cups into a tower. with a 7-DoF robotic arm (Fetch, Fetch Robotics). In an when the human is suboptimal—accelerating through the light—the building the unstable tower was higher, our

5 Collaborative Cup Stacking

Within the autonomous driving user studies, we demonstrated that our Risk-Aware model enables robots to accurately anticipate their human partners. Next, we want to explore how our formalism leverages this accuracy to improve safety and efficiency during HRI. To test the usefulness of our model, we performed two user studies with a 7-DoF robotic arm (Fetch, Fetch Robotics). In an online user study, we verify that the Risk-Aware model can accurately model humans in a collaborative setting. In an in-person user study, the robot leverages Risk-Aware and Noisy Rational models to anticipate human choices and plan trajectories that avoid interfering with the participant. Both studies share a common experimental setup, where the human and robot collaborate to stack cups into a tower.

Experimental Setup. The collaborative cup stacking task is shown in Fig. 1 (also see the supplemental video). We placed five cups on the table between the person and robot. The robot knew the location and size of the cups a priori, and had learned motions to pick up and place these cups into a tower. However, the robot did not know which cups its human partner would pick up.

The human chooses their cups with two potential towers in mind: an efficient but unstable tower, which was more likely to fall, or a inefficient but stable tower, which required more effort to assemble. Users were awarded 20 points for building the stable tower (which never fell) and 105 for building the unstable tower (which collapsed 80% of the time). Because the expected utility of building the unstable tower was higher, our Noisy Rational baseline anticipated that participants would make the unstable tower.

Figure 5: Model accuracy (lower is better) on simulated data. We simulated a spectrum of human action distributions in scenarios where the light often turns red (High risk). The optimal action here is to stop. As the human becomes increasingly optimal, both Noisy Rational and Risk-Aware provide a similarly accurate prediction. But when the human is suboptimal—accelerating through the light—the Risk-Aware autonomous car yields a more accurate prediction.

Summary. We find supporting evidence that Risk-Aware is more accurate at modeling human drivers in scenarios that involve decision making under uncertainty. In particular, our results suggest that the reason why Risk-Aware is more effective at modeling human drivers is because humans often act suboptimally in these scenarios. When humans act rationally, both Noisy Rational and Risk-Aware autonomous cars can understand and anticipate their actions.

5.1 Anticipating Collaborative Human Actions

Our online user study extended the results from the autonomous driving domain to this collaborative cup stacking task. We focused on how accurately the robot anticipated the participants’ choices.

Participants and Procedure. We recruited 14 Stanford affiliates and 36 Amazon Mechanical Turkers for a total of 50 users (32% Female, median age: 33). Participants from Amazon Mechanical Turk had at least a 95% approval rating and were from the United States. After providing informed consent, each of our users answered survey questions about whether they would collaborate with the robot to build the efficient but unstable tower, or the inefficient but stable tower. Before users made their choice, we explicitly provided the rewards associated with each tower, and implicitly gave the probability of the tower collapsing. To implicitly convey the probabilities, we showed videos of humans working with the robot to make stable and unstable towers: all five videos with the stable tower showed successful trials, while only one of the five videos with the unstable tower displayed success. After watching these videos and considering the rewards, participants chose their preferred tower type.

Dependent Measures. We aggregated the participants’ decisions to find their action distribution over stable and unstable towers. We fit Noisy Rational and Risk-Aware models to this action distribution, and reported the log KL divergence between the actual tower choices and the choices predicted by the models.

Hypotheses.

H2. Risk-Aware robots will better anticipate which tower the collaborative human user is attempting to build.

Results. Our results from the online user study are summarized in Fig. 6. During this scenario—where the human is collaborating with the robot—we observed a bias towards risk-averse behavior. Participants overwhelmingly preferred to build the stable tower (and take the guaranteed reward), even though this choice was suboptimal. Only the Risk-Aware robot was able to capture and

3To learn more about our study please check our cup stacking survey link: https://stanfordgsh.qualtrics.com/jfe/form/SV_8ezT04oatQ0ckP
Figure 7: Example robot and human behavior during the collaborative cup stacking user study. At the start of the task, the human reaches for the orange cup (the first step towards a stable tower). When the robot models the human as a Noisy Rational partner (top row), it incorrectly anticipates that the human will build the optimal but unstable tower; this leads to interference, replanning, and a delay. The robot leveraging our Risk-Aware formalism (bottom row) understands that real decisions are influenced by uncertainty and risk, and correctly predicts that the human wants to build a stable tower. This results in safer and more efficient interaction, leading to faster tower construction.

predict this behavior: inspecting the right side of Fig. 6, we found a statistically significant improvement in model accuracy across the board ($t(59) = -21.1$, $p < .001$). Focusing only on the online users, the log KL divergence for Risk-Aware reached $-8.7 \pm 3.0$, while Noisy Rational remained at $-1.3 \pm 0.01$ ($t(29) = -13.1$, $p < .001$). Overall, these results match our findings from the autonomous driving domain, and support hypothesis H2.

5.2 Planning with Risk-Aware Human Models

Having established that the Risk-Aware robot more accurately models the human’s actions, we next explored whether this difference is meaningful in practice. We performed an in-lab user study comparing Noisy Rational and Risk-Aware collaborative robots. We focused on how robots can leverage the Risk-Aware human model to improve safety and efficiency during collaboration.

Participants and Procedure. Ten members of the Stanford University community (2 female, ages 20 – 36) provided informed consent and participated in this study. Six of these ten had prior experience interacting with the Fetch robot. We used the same experimental setup, rewards, and probabilities described at the beginning of the section. Participants were encouraged to build towers to maximize the total number of points that they earned.

Each participant had ten familiarization trials to practice building towers with the robot. During these trials, users learned about the probabilities of each type of tower collapsing from experience. In half of the familiarization trials, the robot modeled the human with the Noisy Rational model, and in the rest the robot used the Risk-Aware model; we randomly interspersed trials with each model. After the ten familiarization trials, users built the tower once with Noisy Rational and once with Risk-Aware: we recorded their choices and the robot’s performance during these final trials. The presentation order for these final two trials was counterbalanced.

Dependent Measures. To test efficiency, we measured the time taken to build the tower (Completion Time). We also recorded the Cartesian distance that the robot’s end-effector moved during the task (Trajectory Length). Because the robot had to replan longer trajectories when it interfered with the human, Trajectory Length was an indicator of safety.

After participants completed the task with each type of robot (Noisy Rational and Risk-Aware) we administered a 7-point Likert scale survey. Questions on the survey focused on four scales: how enjoyable the interaction was (Enjoy), how well the robot understood human behavior (Understood), how accurately the robot predicted which cups they would stack (Predict), and how efficient users perceived the robot to be (Efficient). We also asked participants which type of robot they would rather work with (Prefer) and which robot better anticipated their behavior (Accurate).

Hypotheses.

H3. Users interacting with the Risk-Aware robot will complete the task more safely and efficiently.

H4. Users will subjectively perceive the Risk-Aware robot as a better partner who accurately predicts their decisions and avoids grabbing their intended cup.
Humans display a cognitive bias towards uncertainty and risk—and within these realistic settings, agents. In real-life scenarios, however, humans must make choices not only extended our autonomous driving results to a collaborative human-robot domain, but they also demonstrated how robots can leverage our formalism to meaningfully adjust their behavior and improve safety and efficiency. Our in-lab user study showed that participants interacting with a Risk-Aware robot completed the task faster and with less interference. We are excited that robots can actively use their Risk-Aware model to improve collaboration.

6 Discussion and Conclusion

Many of today’s robots model human partners as Noisy Rational agents. In real-life scenarios, however, humans must make choices subject to uncertainty and risk—and within these realistic settings, humans display a cognitive bias towards suboptimal behavior. We adopted Cumulative Prospect Theory from behavioral economics and formalized a human decision-making model so that robots can now anticipate suboptimal human behavior. Across autonomous driving and collaborative cup stacking environments, we found that our formalism better predicted user decisions under uncertainty. We also leveraged this prediction within the robot’s planning framework to improve safety and efficiency during collaboration: our Risk-Aware robot interfered with the participants less and received higher subjective scores than the Noisy Rational baseline. We want to emphasize that this approach is different from making robots robust to human mistakes by always acting in a risk-averse way. Instead, when humans prefer to take safer but suboptimal actions, robots leveraging our formalism understand these conservative humans and increase overall team performance.

Limitations and Future Work. A strength and limitation of our approach is that the Risk-Aware model introduces additional parameters to the state-of-the-art Noisy Rational human model. With these additional parameters, robots are able to predict and plan around suboptimal human behavior; but if not enough data is available when the robot learns its human model, the robot could overfit. We point out that for all of the user studies we presented, the robots learned Noisy Rational and Risk-Aware models from the same amount of user data. When learning and leveraging these models, the robot must also have access to real-world information. Specifically, the robot must know the rewards and probabilities associated with the human’s decision. We believe that robots can often obtain this information from experience: for example, in our collaborative cup stacking task, the robot can determine the likelihood of the unstable tower falling based on previous trials. Future work must consider situations where this information is not readily available, so that the robot can identify collaborative actions that are robust to errors or uncertainty in the human model.

Finally, we only tested the Risk-Aware model in bandit settings where the horizon is 1. Ideally, we would want our robots to be able to model humans over longer horizons. We attempt to address part of this limitation by conducting a series of experiments in a grid world setting with a longer horizon. We found that a Risk-Aware robot can more accurately model a sequence of human actions as compared to the Noisy Rational robot. Experiment details and results are further explained in the Appendix.

Collaborative robots need algorithms that can predict and plan around human actions in real world scenarios. We proposed an extension of Noisy Rational human models that also accounts for suboptimal decisions influenced by risk and uncertainty. While user studies across autonomous driving and collaborate cup stacking suggest that this formalism improves model accuracy and interaction safety, it is only one step towards seamless collaboration.

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We investigate the effect of both risk and time constraints via this experiment. While it is technically possible for the players to compute the optimal trajectory that leads to the highest expected reward, time limitation makes it very challenging, and humans resort to rough calculations and heuristics. Moreover, we designed the mazes such that humans can get high rewards or penalties if they are in the low-probability (5%) grid. This helps us investigate when humans become risk-seeking or risk-averse.

We recruited 17 users (4 female, 13 male, median age 23), who played both games. We used one game (two grids) to fit the model parameters independently for each user, and the other game (other two grids) to evaluate how well the models can explain the human behavior. As the human actions depend not only the immediate rewards, but also the future rewards, we ran value iteration over the grids and used the values to fit the models as we described in Sec. 3. We again employed Metropolis-Hastings to sample model parameters, and recorded the mean of the samples.

Figure 11 shows the log-likelihoods for each individual user for Risk-Aware and Noisy Rational models. Overall, Risk-Aware explains the test trajectories better. The difference is statistically significant (paired t-test, p < 0.05). In many cases, we have seen risk-averse and risk-seeking behavior from people. For example, 12 out of 17 users chose the risk-seeking action in the test maze by trying to get 25 reward with probability 5% instead of getting 2 with 100% probability. Similarly, 15 out of 17 users choose to guarantee 0.9 reward and gain 0.1 more with 5% probability instead of guaranteeing 1.6 reward and losing 10 with 5% probability. This is an example of suboptimal risk-averse action.