CORONAL NEUTRINO EMISSION IN HYPERCRITICAL ACCRETION FLOWS

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ABSTRACT

Hypercritical accretion flows onto stellar mass black holes (BHs) are commonly believed to be a promising model of central engines of gamma-ray bursts (GRBs). In this model a certain fraction of the gravitational binding energy of accreting matter is deposited to the energy of relativistic jets via neutrino annihilation and/or magnetic fields. However, some recent studies have indicated that the energy deposition rate by neutrino annihilation is somewhat smaller than that needed to power a GRB. To overcome this difficulty, Ramirez-Ruiz and Socrates proposed that high-energy neutrinos from the hot corona above the accretion disk might enhance the efficiency of the energy deposition. We elucidate the disk corona model in the context of hypercritical accretion flows. From the energy balance in the disk and the corona, we can calculate the disk and coronal temperature, $T_D$ and $T_C$, and neutrino spectra, taking into account the neutrino cooling processes by neutrino-electron scatterings and neutrino pair productions. The calculated neutrino spectra consist of two peaks: one by the neutrino emission from the disk and the other by that from the corona. We find that the disk corona can enhance the efficiency of energy release but only by a factor of 1.5 or so, unless the height of the corona is very small, $H \ll r$. This is because the neutrino emission is very sensitive to the temperature of the emitting region, and then the ratio $T_C/T_D$ cannot be very large.

Subject headings: accretion, accretion disks — black hole physics — gamma rays: bursts — neutrinos

1. INTRODUCTION

Gamma-ray bursts (GRBs) are the most explosive phenomena in the universe. Recent developments in the observational study of GRBs and their afterglows have led to the understanding of their emission mechanisms (see Piran 2005; Meszaros 2006 for reviews). The prompt emissions of GRBs are thought to be emitted from optically thin plasmas with highly relativistic velocity in order to avoid the compactness problem (Krolik & Pier 1991; Lithwick & Sari 2001).

Some observational studies show jet breaks in their light curves, implying the relativistic outflow may be anisotropic, or jet (Rhoads 1999; Sari et al. 1999). GRB prompt emission has an energy $E_{\gamma} \sim 10^{51}$ ergs, if we take into account the beaming of the radiation (Frail et al. 2001; Bloom et al. 2003), and the kinetic energy of a relativistic-jet-producing GRB is about $E_{\text{tot}} \sim 10^{52}$ ergs, if we assume the conversion efficiencies of kinetic energy into radiative energy is about 0.1 (Beloborodov 2000; Guetta et al. 2001).

The engines powering such energetic outflows are still unknown. Some long GRBs show associations with Type Ic supernovae, implying that they originate from the core collapse of massive stars (Bloom et al. 1999; Woosley 1993). Short GRBs, on the other hand, have recently been found to be associated with elliptical galaxies (Gal-Yam et al. 2005), so they may originate from neutron star (NS) mergers or black hole–neutron star (BH-NS) mergers (Paczynski 1991; Narayan et al. 1992). As a result of such energetic phenomena, the gravitational energy released in those processes can drive the relativistic jets. A plausible model of the central engine of GRBs involves an accretion disk with extremely high accretion rate ($M \sim 0.01–10 M_{\odot}$ s$^{-1}$) around a stellar mass BH. Such a flow is called a neutrino cooled accretion flow or a hypercritical accretion flow (Kohri & Mineshige 2002). Recent studies of hypercritical accretion flows have been performed by Narayan et al. (1992), Popham et al. (1999), Di Matteo et al. (2002, hereafter DPN02), Kohri et al. (2005), and Kawanaka & Mineshige (2007). The radiative cooling is inefficient in such a hot, dense accretion disk with hypercritical accretion rate, since the optical depth of the disk is so high that photons cannot escape thorough the disk within the accretion timescale. The dominant cooling process of hypercritical accretion flows might be neutrino processes with weak interaction, and the total energy of the neutrino emission reaches some fraction of the rest-mass energy of the accreting matter (DPN02). The gravitational energy is released via neutrino emission, and these neutrinos deposit their energy to the relativistic fireball via neutrino-antineutrino annihilation in the baryon-poor region along the rotational axis. However, some previous work indicated that the energy released via the neutrino process might be insufficient for a GRB. The available energy for deposition by neutrino annihilation is only a few tenths of a percent of the total energy of the emitted neutrinos (Ruffert et al. 1997). DPN02 also pointed out that the energy deposition rate by the neutrino process might be inefficient, since the accretion flow with a high accretion rate becomes thick for neutrinos and generated neutrinos cannot escape from accreting matter (so-called neutrino trapping).

Ramirez-Ruiz & Socrates (2005, hereafter RS05) indicated that nonthermal neutrinos generated in the hot corona (with temperature $T_c$) above the hypercritical accretion disk (with temperature $T_d$) might enhance the energy deposition by neutrino annihilation since the deposition rate is proportional to the mean energy of neutrinos and $T_c$ can be greater than $T_d$. They assumed the coronal depth for neutrinos to estimate the coronal temperature and concluded that the energy deposition rate may increase by some factor if a sufficiently thin corona forms. However, they did not calculate the neutrino spectra and mean energy of the emitted neutrinos. Moreover, the coronal region they assumed may be too small, and thus the coronal temperature might have been overestimated.

In this paper we elucidate the disk corona model in the context of the hypercritical accretion scenario and show that the
mean energy of emergent neutrinos from hypercritical accretion flows is enhanced by the existence of a neutrino-thin corona. We take a reasonable value of the coronal thickness and calculate the emergent spectra of neutrinos from the corona. In § 2 our model of the disk corona is described with some adopted assumptions. We show the numerical method to calculate the neutrino spectra, and energy equations to determine the temperature of the corona and the disk are written in § 3. We consider the absorbed neutrinos by the dense disk, which reemits thermal neutrinos, to determine the coronal temperature self-consistently, which RS05 did not take into account. Then we present our results in § 4 and discuss the possibility of the corona enhancing the energy deposition rate in § 5.

2. OUR MODEL

We first outline our model in this section. The disk corona model was originally developed to explain the nonthermal spectral component of X-ray binaries and active galactic nuclei (AGNs) in analogy with the model for the solar corona (see, e.g., Shibata et al. 1990). From the fitting to the observed spectra it has become clear that $f$, the fraction of gravitational energy released in diffuse corona, should be almost unity; i.e., almost all the liberated gravitational energy should be dissipated in the corona, since otherwise the large flux of the nonthermal spectral component, which is comparable with that of the thermal component, cannot be explained (Haardt & Maraschi 1991). The magnetic pressure can be amplified up to the equipartition value with the gas pressure by MHD processes, such as magnetorotational instability in the accretion disk (Balbus & Hawley 1998; Machida & Matsumoto 2003). Magnetic loops are formed and lifted up by the Parker instability, creating a corona filled with magnetic fields (Galeev et al. 1979; Stella & Rosner 1984). This corona may be heated by magnetic reconnection. In this way some fraction $f$ of the total gravitational energy can be released in the corona. Liu et al. (2002) have shown that $f \sim 1$ from the consideration of energy balance in the disk corona system.

A hot corona might also form in hypercritical accretion flows since the accretion disk is highly turbulent (RS05). Thus, we follow the ordinary disk corona model mentioned above to construct the disk corona model in the context of hypercritical accretion flows for GRBs. The high-energy neutrinos from the hot corona can enhance the energy deposition rate by neutrino annihilation, since the annihilation cross section cross section depends on the energy of neutrinos. The energy deposition rate by neutrino annihilation per unit volume is (Ruffert et al. 1997)

$$q_{\nu \bar{\nu} \rightarrow e^+ e^-} = \frac{2(C_{\nu e}^2 + C_{\nu e}^4)}{3\pi} G_F^2 \times \int d\Omega_\nu \int d\Omega_\bar{\nu} (\langle E_\nu \rangle + \langle E_{\bar{\nu}} \rangle) I_{\nu} I_{\bar{\nu}} (1 - \cos \theta)^2,$$

where $C_{\nu e} = \frac{1}{2} + 2 \sin^2 \theta_W$ and $C_{\nu e} = \frac{1}{2}$ for electron-type pairs, $C_{\nu e} = \frac{1}{2} + 2 \sin^2 \theta_W$ and $C_{\nu e} = \frac{1}{2}$ for heavy-lepton neutrino pairs, $G_F$ is the Fermi coupling constant, $\langle E_\nu \rangle = \int E I_\nu(E) dE / \int I_\nu(E) dE$ [or $\langle E_{\bar{\nu}} \rangle = \int E I_{\bar{\nu}}(E) dE / \int I_{\bar{\nu}}(E) dE$] is the mean energy of neutrinos (antineutrinos), $I_{\nu}$ (or $I_{\bar{\nu}}$) is intensity of emitted neutrinos (antineutrinos), $\theta$ is the collision angle, and $\Omega_\nu$ (or $\Omega_{\bar{\nu}}$) is the solid angle of neutrino (antineutrino) emission, which depends on the geometry of the emitting region. We take the Weinberg angle, $\theta_W$, as $\sin^2 \theta_W = 0.23$. For simplicity, we assume that neutrinos and antineutrinos are all electron type and have the same intensity. Thus, the energy deposition rate is roughly proportion to the mean energy of neutrinos. If the hot corona forms, then the neutrino spectra, which are generally assumed as thermal, may be deformed and have a higher mean energy than the original value.

The energy released in the accretion disk per unit surface can be calculated by using the standard disk theory and is written as (Kato et al. 1998)

$$Q^+ = \frac{3GM\dot{M}}{8\pi r^2} \left( 1 - \sqrt{\frac{r_{in}}{r}} \right).$$

where $M$, $\dot{M}$, and $r_{in}$ are the mass of the black hole, the accretion rate, and the inner boundary radius of the accretion disks where the torque vanishes, respectively. We take $M = 3 M_\odot$ and $r_{in} = 3r_S \sim 3 \times 10^6$ cm, where $r_S$ is the Schwarzschild radius. If the neutrino cooling is efficient, this dissipated energy is released as neutrino emission. We consider a plane-parallel and homogeneous corona with vertical thickness $H$ above the disk (Fig. 1). We conservatively assume that the parameter value $H$ is comparable with the disk thickness, since the most unstable wavelength of the Parker instability is nearly the scale height in the disk (e.g., Matsumoto et al., 1988), and thus the typical scale of the magnetic field in the corona would be comparable to the scale height.

Neutrino emission from the inner part of the disk dominates over that from the outer part and mainly contributes to the heating of the relativistic fireball above the disk. Then we evaluate the enhancement of the mean energy of the neutrinos at $r = 4r_S$, where the energy dissipation rate nearly reaches its maximum value, and we assume that this enhancement is proportional to that of the total energy deposition rate by neutrino annihilation. We assume that the corona consists of pure relativistic electron-positron plasma since the corona may form above the surface of the disk where the density of baryons is much less than that inside the disk (discussed below). We also assume that the electrons and positrons are completely thermalized, since the timescale of electromagnetic interactions is much shorter than that of weak interactions by many orders of magnitude.

As the coronal cooling processes we take into account neutrino reactions as

$$\nu + e^+ \rightarrow \nu + e^+, \quad (3)$$
$$e^- + e^+ \rightarrow \nu + \bar{\nu}. \quad (4)$$
The thermal neutrinos emitted from the disk are upscattered by hot electrons and positrons in the corona. The scattered neutrinos have higher energy since the temperature of the corona \( T_c \) is higher than that of the disk \( T_d \), and hence the emerged neutrino spectrum is deformed. The corona is cooled via scatterings of neutrinos by high-energy electrons and positrons in the corona. Some part of the scattered neutrinos is reabsorbed and heats the disk, which reemits thermal neutrinos. Neutrino pairs produced by annihilation of high-energy electrons and positrons in the corona also cool the corona and have high-energy spectra. We neglected the scattering of neutrinos produced by pair process in the corona because the energy of the neutrinos emitted in the corona is almost the same energy as that of hot electrons and because the optical depth of electron-neutrino scattering is much less than unity in the corona. We also neglected the Fermi blocking effect by the background of electrons, positrons, and neutrinos.

On the basis of these assumptions, we can calculate \( T_d \) and \( T_c \) by solving energy equations including neutrino processes, which are needed to calculate the neutrino spectra (see § 3.3).

### 3. CALCULATIONS OF NEUTRINO SPECTRA

Hereafter we take the units as \( c = 1 \), \( h = 1 \), and \( k = 1 \). Calculating the neutrino spectrum emitted from the disk corona system is important when we evaluate the energy deposition rate by neutrino annihilation, since the deposition rate is proportional to the neutrino energy. In this section we present the method to calculate the coronal neutrino spectra and their mean energy.

#### 3.1. Neutrino-Electron Scattering

We calculated the change of energy of neutrinos upscattered by hot coronal electrons and positrons. The differential cross section of neutrino-electron scattering is \( \langle \text{'t Hooft} 1971; Kneller et al. 2006 \rangle \)

\[
\frac{d\sigma_{\nu e}}{dK_{\nu e}} = G_F^2 m_e^2 \begin{pmatrix} C_V + C_A \end{pmatrix}^2 \begin{pmatrix} C_V - C_A \end{pmatrix}^2 \left( 1 - \frac{K_{\nu e}}{E_{\nu e}} \right)^2 - \left( C_V^2 - C_A^2 \right) \frac{m_e K_{\nu e}}{E_{\nu e}},
\]

where \( C_V = \frac{1}{2} + 2 \sin^2 \theta_W \) and \( C_A = \frac{1}{2} \) for electron-electron neutrino scattering, \( C_V = \frac{1}{2} + 2 \sin^2 \theta_W \) and \( C_A = -\frac{1}{2} \) for positron-electron neutrino scattering, \( K_{\nu e} \) is the kinetic energy of a recoiled electron, and \( E_{\nu e} \) is the energy of an incident neutrino in the rest frame of the electron. We do not deal here with the composition of neutrino flavors, since the detailed composition depends on the structure of the disk. We assume that the emitted neutrinos from the disk are all electron type since nucleon pair capture is a dominant neutrino process in the disk.

The mean free path, \( \lambda \), of neutrinos in the corona for neutrino-electron scattering is then (Landau & Lifshits 1975)

\[
\lambda^{-1} = \frac{2}{(2\pi)^3} \int \sigma_{\nu e}(1 - \mu \beta) f_e d^3 p,
\]

where \( \beta, p, \) and \( f_e \) are the velocity, momentum, and distribution function of electrons, respectively, and \( \mu \) is cosine of the angle between the directions of the neutrino and electron. We assume that the corona consists of pure electron-positron plasma in thermal equilibrium by electromagnetic process so that the distribution function of a pair should be Fermi-Dirac type, \( f_e = \left\{ \exp \left( \frac{p^2 + m_e^2}{2T_c} \right) + 1 \right\}^{-1} \) in the relativistic limit, where \( T_c \gg m_e \), the total coronal depth for neutrino-electron scattering is

\[
\tau \equiv \frac{H}{\lambda} \approx 0.27 \frac{H}{10^6 \text{ cm}} \left( \frac{E_{\nu}}{10 \text{ MeV}} \right)^4 \left( \frac{T_c}{10 \text{ MeV}} \right)^4,
\]

where \( E_{\nu} \) is the energy of the incident neutrino in the laboratory frame. Hence, higher energy neutrinos have more chances to collide with coronal electrons than lower energy ones.

We calculate the neutrino spectra scattered by coronal electrons and positrons by using a Monte Carlo method, following Pozdnyakov et al. (1977) and Liu et al. (2003). We first set the weight of a neutrino as \( w_0 = 1 \) for a given thermal neutrino with energy, \( E_{\nu} \), which has the Fermi-Dirac distribution. We calculate the probability of neutrinos passing through the corona, \( P_0 = \exp \frac{-\mu}{\cos \alpha} \), where \( \alpha \) is the angle between the neutrino direction and the z-axis, which is perpendicular to the coronal plane. Then \( w_{n+1} = w_{n-1} \) is the transmitted portion of neutrinos and the remaining \( w_1 = w_0(1 - P_0) \) is the portion of neutrinos scattered at least once. Let \( w_{n+1} = w_{n-1}(1 - P_{n-1}) \) be the portion of neutrinos experiencing the \( nth \) scattering. We continue the calculation until the weight, \( w_n \), becomes sufficiently small. By repeating the same procedures for a sufficiently large number of neutrinos, we can calculate emergent spectra by collecting neutrinos going upward through the coronal surface at \( z = H \), while downward neutrinos crossing the lower boundary are reabsorbed by the disk body, thereby heating the disk.

#### 3.2. Neutrino-Antineutrino Pair Production

We also calculate the neutrino pair emission by weak interaction in the pair plasma. The cross section for pair production is (Dicus 1972; Yakovlev et al. 2001)

\[
\sigma_{\nu^- e^+ \rightarrow \bar{\nu}^- \bar{\nu}^+} = \frac{G_F^2}{12\pi} \frac{m_e^4}{E_1 E_2}
\]

\[
\times \left\{ \left( C_V^2 + C_A^2 \right) \left[ 1 + 3 \frac{P_1 \cdot P_2}{m_e^2} + 2 \left( \frac{P_1 \cdot P_2}{m_e^2} \right)^2 \right]
\]

\[
+ 3 \left( C_V^2 - C_A^2 \right) \left[ 1 + 2 \frac{P_1 \cdot P_2}{m_e^2} \right] \right\}.
\]

where \( C_V = \frac{1}{2} + 2 \sin^2 \theta_W \) and \( C_A = \frac{1}{2} \) for pair production of electron types, \( C_V = -\frac{1}{2} + 2 \sin^2 \theta_W \) and \( C_A = -\frac{1}{2} \) for pairs of \( \mu^- \) and \( \tau^- \) neutrinos, \( E_1 \) (or \( E_2 \)) and \( P_1 \) (or \( P_2 \)) are the energy and four-momentum of electrons (positrons), respectively, and \( r \) is the relative velocity of the pair. The neutrino pair emissivity is given as

\[
q_{e^- e^+ \rightarrow \bar{\nu}^- \bar{\nu}^+} = \frac{4}{(2\pi)^3} \int d^3 p_1 d^3 p_2 \left( E_1 + E_2 \right) \sigma_{\nu^- e^+ \rightarrow \bar{\nu}^- \bar{\nu}^+} f_1 f_2.
\]

We assume that the distribution functions of electrons and positrons are Fermi-Dirac type with the same temperature, \( T_c \). In the relativistic limit where \( T_c \gg m_e \), the total emissivity becomes

\[
q_{e^- e^+ \rightarrow \bar{\nu}^- \bar{\nu}^+} = 1.39 \times 10^{34} \left( \frac{T_c}{10 \text{ MeV}} \right)^9 \text{ ergs cm}^{-3} \text{ s}^{-1}.
\]
and the mean energy of neutrinos is

\[ \langle E \rangle = \frac{\int d^3p_1 d^3p_2 E_1^2 \sigma_{\nu\nu} f_1 f_2}{\int d^3p_1 d^3p_2 E_1 \sigma_{\nu\nu} f_1 f_2} \]
\[ \simeq 5.1 T_c. \quad (11) \]

Half of the emitted neutrinos pass upward through the corona, and the remaining half are absorbed and heat the disk since emission of the pair process is isotropic. The emissivity, equation (10), includes all types of neutrinos, but we assume that the emitted neutrinos by pair process are only electron type when considering heating of the disk by downward neutrinos and the energy deposition to the relativistic fireball by upward neutrinos. This is a reasonable assumption in doing a simple estimation, since the ratios of the emissivity of each type of neutrino are, from equation (9), 0.70:0.15:0.15 for \( \nu_e: \bar{\nu}_e: \nu_x \).

We also calculated the neutrino spectra from the pair process by the Monte Carlo method. The reaction rate of electron-positron annihilation by weak interaction is given as

\[ \frac{d\sigma_{e^+ e^- \rightarrow \nu \bar{\nu}}}{d\Omega} \propto |M|^2 \]
\[ = 8G_F^2 \left[ (C_V - C_A)^2 P_1 \cdot Q_1 P_2 \cdot Q_2 + (C_V + C_A)^2 P_2 \cdot Q_1 P_1 \cdot Q_2 + m_e^2 (C_V^2 - C_A^2) Q_1 \cdot Q_2 \right], \quad (13) \]

where \( P_1 \) (or \( P_2 \)) and \( Q_1 \) (or \( Q_2 \)) are the four-momentum of electrons (positrons) and neutrinos (antineutrinos), respectively, and \( |M|^2 \) is the amplitude of the pair process. We determined the emitted energy of neutrino pairs with reaction weight \( w \) from the differential cross section formula and calculated the neutrino spectra from the pair process.

3.3. Energy Balances in the Corona and the Disk

We calculate the temperature of the corona and that of the disk consistently by solving their energy balances simultaneously and by calculating the neutrino spectra (see Fig. 2). We assume that the fraction \( f \) of the total energy is dissipated in the corona and the remaining part, \( 1 - f \), in the disk, neglecting the advection of energy. The energy balance in the disk is

\[ (1 - f) Q^+ + Q_{\text{ref}} + \frac{1}{2} q_{e^+ e^- \rightarrow \nu \bar{\nu}} H = \frac{7}{8} \sigma T_d^4, \quad (14) \]

where we assumed that the corona is thin for neutrinos emitted by pair process so that we can neglect the absorptions by the inverse pair process. On the other hand, the energy balance in the corona is

\[ f Q^+ + \frac{7}{8} \sigma T_d^4 = Q_{\text{esc}} + Q_{\text{ref}} + q_{e^+ e^- \rightarrow \nu \bar{\nu}} H, \quad (15) \]

where \( Q_{\text{esc}} \) is the cooling rate by the thermal neutrinos from the disk and upward neutrinos scattered by electrons and positrons, and \( Q_{\text{ref}} \) is that by the downward scattered neutrinos, which can be evaluated by calculating the scattered neutrino spectra. If all of the energy is dissipated within the disk, i.e., when \( f = 0 \), the effective temperature of the disk at \( r = 4 r_s \) is

\[ T_{d,0} = 4.2 \left( \frac{M}{3 M_\odot} \right)^{-1/2} \left( \frac{\dot{M}}{1 M_\odot \text{s}^{-1}} \right)^{1/4} \text{MeV}, \quad (16) \]

and the mean energy of thermal neutrinos from the disk is \( \langle E \rangle_0 \simeq 4.1 T_{d,0} \).

4. RESULTS

4.1. Neutrino-Electron Scattering

First we consider the effect of scattering alone as a cooling mechanism of the corona in analogy with the coronae of standard accretion disks in X-ray binaries and AGNs. From equations (14) and (15), and neglecting the pair process, we can calculate the temperature of the corona and the disk by iteratively calculating the change of neutrino energy \( Q_{\text{esc}} \) and \( Q_{\text{ref}} \) by the Monte Carlo method. Figure 3 shows the coronal and disk temperatures for \( M = 1 M_\odot \text{s}^{-1} \) as functions of \( f \). A thinner corona (with smaller \( \tau \)) has a higher temperature for a given \( T_d \), since the cooling rate of the corona by scatterings is roughly written as

\[ f Q^+ \sim \frac{7}{8} \sigma T_d^4 \tau T_d, \quad (17) \]

where we assume that the scattered neutrino has nearly the same energy as that of electrons, and that \( \tau \) is proportional to the thickness of the corona.

We then show the neutrino spectra where \( f \) is close to unity (Fig. 4, left). The neutrino spectra have two components: thermal neutrinos from the disk and scattered neutrinos in the hot corona. Nearly half of the scattered neutrinos go downward and are absorbed by the disk, which generates soft thermal neutrinos, and the remaining half pass upward producing a high-energy spectrum. Once the thermal neutrinos are scattered, they acquire energy nearly equal to that of the coronal electrons, since the
energy of the neutrino is too high \( T_d \gtrsim m_e \) to be scattered elastically. The high-energy part of the emergent neutrino spectra mainly contributes to neutrino heating by neutrino annihilation. If \( H \) is on the same order as \( r \), in contrast, the coronal temperature is not significantly high compared with disk temperature. Thus, the effect of upscattering is small and the spectrum does not show two humps so clearly.

We also calculate the mean energy of neutrinos from neutrino spectra, and the amplification of the neutrino mean energy is shown in Figure 4 (right). With a conservative value of the coronal thickness, \( H/r \sim 0.1-1 \), the amplification factor of the mean energy is about a factor of 2.

### 4.2. Neutrino Pair Production

In the next case we take into account the effect of cooling by neutrino pair production. By neglecting the scattering, the temperature of the corona and the disk can be solved analytically. The temperature of the corona and the disk at \( r = 4r_S \) are

\[
T_c = 5.6f^{1/9} \left( \frac{M}{3M_\odot} \right)^{-1/3} \left( \frac{\dot{M}}{1M_\odot \text{ s}^{-1}} \right)^{1/9} \left( \frac{H}{r} \right)^{-1/9} \text{ MeV},
\]

(18)

\[
T_d = 4.2 \left( 1 - \frac{f}{2} \right)^{1/4} \left( \frac{M}{3M_\odot} \right)^{-1/2} \left( \frac{\dot{M}}{1M_\odot \text{ s}^{-1}} \right)^{1/4} \text{ MeV},
\]

(19)

and the mean energy of the emergent neutrinos is \( \langle E \rangle \simeq 4.1T_d \times (1 - f/2) + 5.1T_c f/2 \).

We also solved equations (14) and (15), and evaluated \( T_d \) and \( T_c \), including the effects of scatterings. Figure 5 shows the temperatures in the cases with \( \dot{M} = 1M_\odot \text{ s}^{-1} \). The effect of neutrino-electron scattering is negligible, and the behavior of the temperature is well described by equations (18) and (19).

The emerged neutrino spectra with neutrino-electron scatterings and pair process are shown in Figure 6 (left). Note that the effect of scatterings is so small that scattered neutrinos make a small hump at the electron energy, which is overlaid by the spectrum of the pair process. In the case where \( f \sim 1 \), half of the energy dissipated in the corona is reprocessed in the disk as thermal neutrinos with lower temperature, and the half emitted by pair process with higher temperature pass through the neutrino-thin...
corona. Figure 6 (right) shows the amplification of neutrino mean energy, including the scattering and pair process. If we take $H/r = 0.1$, the mean energy of neutrinos is enhanced by a factor of about 1.5. A thinner corona becomes hotter and emits neutrinos with higher energy because the neutrino emission should occur in a small dissipation region to cool the corona.

4.3. $M$ Dependence

There is a hope that $T_c$ may increase with an increase of $M$ so that the energy amplification factor could increase as $M$ increases.

Therefore, we also calculated the amplification of the mean energy of neutrinos in the cases where $M = 0.1$ and $10 M_\odot \, \text{s}^{-1}$. From Figure 7 we see that the mean energy of neutrinos from the corona with high accretion rate tends to be slightly enhanced since the $M$ dependence of the coronal temperature is weak. In the case with $M = 0.1 M_\odot \, \text{s}^{-1}$ the mean energy of neutrinos is enhanced by a factor of 2 with $H = 0.1 r$, but the neutrino luminosity (and the absolute value of mean energy) is small. On the other hand, when $M = 10 M_\odot \, \text{s}^{-1}$, the mean energy is enhanced only by a factor of 1.2 even though we neglect the effect of neutrino trapping. If we consider neutrino trapping, the enhancement will be smaller. Thus, there is practically no improvement in the neutrino energy, even if $M$ is larger.

5. SUMMARY AND DISCUSSION

5.1. Brief Summary

A magnetically heated corona above the accretion disk may emit nonthermal, high-energy neutrinos, which, in principle, would lead to an enhancement of the energy deposition rate by neutrino annihilation. The improvement is, however, only by a factor of 2 or so when $H/r \gtrsim 10^{-3}$. Hence, the energy deposition might still be insufficient to energize GRBs unless $H/r$ is extremely small. We see that a higher energy of neutrinos is expected if the corona forms in a thinner region compared to the disk scale height.

We also see that the effect of the scattering between electrons and neutrinos is negligible compared with the cooling by pair process. The ratio of the energy loss rate of the corona by electron-neutrino scatterings to the emission rate from the corona by pair process is approximately

$$\frac{(7 \sigma T_d^4/8)(T_c/T_d)\tau}{q_{\nu e} H} \approx 0.1 \left(\frac{T_d}{T_c}\right)^4,$$

Then the effect of scattering is negligible at the higher coronal temperature, which is the situation which we are considering. We can easily understand this ratio by considering the temperature.
dependences of the two processes with neutrinos. The number density of coronal electrons is roughly $n_e \propto T_c^3$, and the cross section for pair process is $\sigma_{e^+e^-\to \nu\bar{\nu}} \propto T_c^2$; thus, the emissivity of neutrino pair production is proportional to $T_c^3 \sigma_{e^+e^-\to \nu\bar{\nu}} n_e^2 \propto T_c^9$. On the other hand, the number density of thermal neutrinos is $n_\nu \propto T_d^3$, and the cross section for electron neutrino scattering is $\sigma_{\nu e} \propto T_d^4 T_c$. Hence, the emissivity of neutrinos scattered by coronal electrons is proportional to $T_d^4 T_c^3 \sigma_{\nu e} n_\nu \propto T_d^7 T_c$, where we assume that the energy of scattered neutrinos is roughly $T_c$.

From these simple estimations, we understand that the emission of the pair process dominates that of electron neutrino scatterings by a factor of $(T_c/T_d)^{9/2}$.

From Figure 5, we see that the temperature of the disk does not decrease so much even if $f$ increases. This can be understood in the following way: since about half of the energy of the emitted neutrinos in the corona is absorbed and heats the disk, more than a half of the gravitational energy, $Q^+$, is emitted as thermal neutrinos from the disk. Hence, the disk temperature decreases by only a factor of $0.5^{1/4} \sim 0.84$ even if $f \sim 1$ (the case in which most of the gravitational energy is dissipated in the corona), compared with the cases without disk corona.

We also investigated the dependence of the mean energy of the neutrinos on the accretion rates. The disk temperature $T_{d,0}$ is proportional to $M^{1/4}$ since the dissipative energy is proportional to $M$, while the coronal temperature is proportional to $M^{1/6}$ if the pair process dominates. Hence, the ratio $T_c/T_{d,0}$ is proportional to $M^{-5/36}$. Although the neutrino luminosity is proportional to $M$, even if we neglect the advective energy by neutrino trapping in the disk, the enhancement of the mean energy of the neutrinos is small at high accretion rates. Thus, we cannot expect significant enhancement of neutrino heating by high-energy neutrinos even at high accretion rates. If we take neutrino trapping into account, we need to divide the fraction of energy dissipated in the disk, $1-f$, by $1-f-f_{\text{adv}}$, where $f_{\text{adv}}$ is the fraction of advective energy. We could neglect the advective energy when $f \sim 1$ since the energy is transported via the magnetic process to the surface of the disk on the dynamical time-scale, which is shorter than the neutrino diffusion time (Ohsuga et al. 2002). This will lead to improvement of the result of DPN02 even though the enhancement of the mean energy of neutrinos may still be small.

5.2. Confinement of Coronal Plasma

The corona might be formed by the energy release of magnetic fields in a thin region above the disk. What can then confine the magnetic corona? If we consider the hydrostatic balance in the corona, the thickness of the corona becomes

$$H \sim \frac{c_s}{\Omega_K} \sim \sqrt{\frac{2}{3}} \left(\frac{r}{r_s}\right) r > r_s,$$

(21)

where we assumed the sound speed in the corona to be $c_s = 1/\sqrt{3}$. Hence, the corona cannot be gravitationally bound but expands, unless the radial position of the corona is very close to the Schwarzschild radius. The ratio of the cooling time, $t_{\text{cool}} \sim 11aT_c^{5/2}/4d_{e^+e^-\to \nu\bar{\nu}}$, to the free expansion time of the corona, $t_{\exp} \sim H/c_s$, is

$$\frac{t_{\text{cool}}}{t_{\exp}} \sim \frac{22}{7\sqrt{3}} \tau_{\nu e}^{-1} > 1,$$

(22)

where $\tau_{\nu e} = q_{e^+e^-\to \nu\bar{\nu}} H/4(7/8)\sigma T_c$ is the neutrino optical depth of the corona for the pair process (RS05). Thus, the corona should expand before the coronal plasma is cooled by neutrino emission since we now consider the neutrino-thin hot corona, and some processes are needed to confine the coronal plasma in a thin region.

The magnetic pressure could be amplified up to the equipartition value of the gas pressure in the disk and the amplified magnetic fields would be lifted up in the corona (RS05). Such strong magnetic fields in the corona might be able to confine the coronal plasma if the magnetic pressure is higher than that of relativistic particles in the corona. Since the gas pressure in the disk is roughly $P_{\text{gas}} \sim 10^{36}$ ergs cm$^{-3}$ for $M = 1 M_\odot$ s$^{-1}$ (DPN02), the magnetic fields, whose pressure is comparable to $P_{\text{gas}}$, could...
confine the corona if $T_c \lesssim 10$ MeV, i.e., $H \gtrsim 10^{-3}r$ in our model (see Fig. 5). Our estimates above include some uncertainties, e.g., the detailed structure of the magnetic fields, and we need further studies to see whether such magnetic fields really can confine the coronal plasma.

5.3. Baryon Contamination in the Corona

Finally, we discuss the validity of the assumption that the corona consists of pure pair plasma with negligible baryons. In the existence of baryons, neutrino emission by the pair capture process may also cool the corona. The cooling rate by the pair capture process dominates over that by the pair process if the corona contains a sufficient amount of baryons, $\rho_{10} > 0.6 T_{c10}^3$, where $\rho_{10}$ is the density of baryons in units of $10^{10}$ g cm$^{-3}$ and $T_{c10} = T_c/10$ MeV (Popham et al. 1999). Thus, for the validity of the assumptions in our model, the baryon density in the corona should be smaller than that in the dense disk, whose baryon density is typically $10^{10}-10^{11}$ g cm$^{-3}$ for a neutrino-thick disk (e.g., Kawanaka & Mineshige 2007). Since the coronal temperature is $T_{c10} \lesssim 1$ with a moderate thickness of the corona in our model, $H \gtrsim 10^{-3}r$, the baryon density in the corona should be less than that in the disk by 1 or 2 orders of magnitude. This condition could be marginally justified.

Moreover, the distribution function of electrons in the corona could be deformed from the Fermi-Dirac type of zero chemical potential. In such a case the neutrino emission by the pair process could be suppressed (Kohri & Mineshige 2002). Since the chemical potential of electrons is determined by the amount of baryons in the corona, this calculation is beyond the scope of this work and should be done in future work.

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