Molecular dynamics simulations of Y(III) coordination and hydration properties

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Y mainly exists in ionic rare-earth resources. During rare-earth carbonate precipitation, rare-earth ion loss in the precipitated rare-earth mother liquor often occurs due to CO$_3^{2-}$ coordination and Y(III) hydration. Microscopic information on the coordination and hydration of CO$_3^{2-}$ and H$_2$O to Y(III) has not yet been elucidated. Therefore, in this study, the macroscopic dissolution of Y(III) in different aqueous solutions of Na$_2$CO$_3$ was studied. The radial distribution function and coordination number of Y(III) by CO$_3^{2-}$ and H$_2$O were systematically analyzed using molecular dynamics (MD) simulations to obtain the complex ion form of Y(III) in carbonate solutions. Density functional theory (DFT) was used to geometrically optimize and calculate the UV spectrum of Y(III) complex ions. This spectrum was then analyzed and compared with experimentally determined ultraviolet-visible spectra to verify the reliability of the MD simulation results. Results showed that Y(III) in aqueous solution exists in the form of [Y·3H$_2$O]$^+$ and that CO$_3^{2-}$ is present in the bidentate coordination form. In 0–0.8 mol L$^{-1}$ CO$_3^{2-}$ solutions, Y(III) was mainly present as the 5-coordinated complex [YCO$_3$·3H$_2$O]$^+$. When the concentration of CO$_3^{2-}$ was increased to 1.2 mol L$^{-1}$, [YCO$_3$·3H$_2$O]$^+$ was converted into a 6-coordinated complex [YCO$_3$·2H$_2$O]$^+$. Further increases in CO$_3^{2-}$ concentration promoted Y(III) dissolution in solution in the form of complex ions. These findings can be used to explain the problem of incomplete precipitation of rare earths in carbonate solutions.

1. Introduction

The demand for elemental Y has increased yearly due to its excellent optical applications. Rare-earth carbonates are important inorganic salts used in the extraction and application of rare-earth elements.$^{1}$ Y mainly exists in ionic rare-earth resources and xenotime, and the solubility of Y and Ln carbonates in water is merely 10$^{-5}$ to 10$^{-7}$ mol L$^{-1}$; therefore, carbonate is used in the industry to precipitate rare-earth ions.$^{2-4}$ However, rare-earth ions in the mother liquor are considerably lost due to the coordination and hydration in the carbonate solution. The microscopic information of the coordination and hydration by CO$_3^{2-}$ and H$_2$O on rare-earth ions has not been elucidated.$^{5,6}$

From the 1970s to the 1990s, many scholars have researched the solubility and complex ion morphology of Ln elements in carbonate solution. The amount of Ln dissolved in Na$_2$CO$_3$ solution and the ion morphology are mainly related to the concentration of CO$_3^{2-}$. Taketatsu$^{7,8}$ studied the solubility of rare-earth elements in different concentrations of K$_2$CO$_3$ solution and showed that the dissolved amount of rare-earth elements in K$_2$CO$_3$ solution increases with the carbonate concentration and the atomic number (except for Ce, Y, and Sc). Tran$^9$ investigated the geological migration of Ce in fractured carbonate rock formations and found that in a groundwater environment with pH 7–9, the main rare-earth carbonate complex ions are RECO$_3$$^+$ and RE(CO$_3$)$_2^-$; complex ions, such as REHCO$_3$$^-$ and REOH$^+$, are nearly negligible. In a study on low concentration CO$_3^{2-}$ natural groundwater, Noack et al.$^{10}$ found that heavy rare-earth elements (HREEs) are more easily coordinated with CO$_3^{2-}$ than light rare-earth elements (LREEs) and produce RE(CO$_3$)$_2^-$.

Johannesson$^{11,12}$ researched the geochemical behavior of CO$_3^{2-}$ and RE$^{3+}$ in Mono Lake water; the forms of rare-earth carbonate complex ions are RE(CO$_3$)$_2^-$ at 0.27 M CO$_3^{2-}$ in lake water and RECO$_3$$^+$ in lower-concentration CO$_3^{2-}$ groundwater. Philippini$^{13,14}$ found that RE(CO$_3$)$_2^-$, RE(CO$_3$)$_3$$^{3-}$, and other complex ions exist in aqueous solutions with different CO$_3^{2-}$ concentration gradients (0.1–1.5 mol L$^{-1}$). In summary, the complexation mode and morphology of rare-earth ions change with the concentration of CO$_3^{2-}$.

Reiller et al.$^{15,16}$ performed inductive analysis of the existing migration of Am and associated it with rare-earth elements; they concluded that when the pH of the solution is less than 7, between 7 and 8.5, and above 8.5, the main complex ions are RE$^{3+}$, RECO$_3$$^+$, and RE(CO$_3$)$_2^-$, and possibly RE(CO$_3$)$_3$$^{3-}$ or higher-valence-state complex ions, respectively. Given
similarities in the physicochemical properties of Am and rare-earth elements, Maloubier et al. investigated the results of Am migration studies and concluded that the main forms of rare-earth carbonate ions in a water environment with pH 7–9 are RECO$_3^-$ and RE(OCO$_2$)$_3$$. This work thus indicated that the morphology of rare-earth complex ions is also related to the pH of the solution.

Using available crystallographic and spectral data, including ultraviolet-visible (UV-vis), near-infrared, and infrared spectra, Jeanvoine stated that all Ln$^{(n)}$ ions form tetra-carbonate ions in aqueous solution when carbonate ions are not restricted. Philippi et al. used electrophoretic mobility shift and time-resolved laser-induced fluorescence spectroscopy (TRLFS) to study several Ln$^{(n)}$–carbonate complexes and concluded that light rare-earth Ln$^{(n)}$ ions can coordinate 4 carbonate ligands, whereas heavy rare-earth Ln$^{(n)}$ can only coordinate with 3.

Modern research methods have enabled significant advances in the analysis of the forms of ions in rare-earth carbonate solutions, but nearly all available studies involved are extrapolated analyses of different rare-earth carbonates. The structures of rare-earth complex ions in carbonate aqueous solutions are complex and diverse, and their specific forms remain unclear; thus, difficulties have been encountered when directly using UV-vis, near-infrared, infrared, X-ray, and TRLFS to clarify the structure of rare-earth-complex ions.

Martelli et al. achieved remarkable results through polarization MD simulation studies and examined the structure and kinetics of tri-and tetra-carbonate complexes. Jeanvoine et al. used the density functional theory (DFT) method to study the bonding theory of Ln$^{(n)}$ tri- and tetra-carbonate ions and provided the following conclusions: (1) in the gas phase, the most stable structures are full bidentate and monodentate for tri- and tetra-carbonate complexes, respectively; (2) in the aqueous phase, when the interaction of water molecules is not explicitly considered in the continuous model, the full bidentate complexes are the most stable structures; and (3) Ln$^{(n)}$–carbonate interactions mainly occur through ionic bonds.

After decades of development in the field of rare-earth metals, many scholars have studied the macroscopic dissolution of aqueous solutions in rare-earth elements in carbonates. However, studies on the microstructure and coordination behavior with CO$_3^{2-}$ and H$_2$O in carbonate solution are scarce. Therefore, the coordination and hydration microscopic information of Ln$^{(n)}$ ions must be further examined.

Y and Ln do not belong to the same period in the periodic table of elements, and their atomic and ionic electronic layer structures considerably differ. However, the properties of Y are substantially similar to those of heavy rare-earth elements, and this similarity requires deep understanding. Therefore, the dissolution law of Y and the microscopic information of its coordination and hydration should be investigated. Motivated by previous studies on the dissolution of Ln elements and complex ion morphology, in the present work, we studied the microscopic interaction of Y with CO$_3^{2-}$ and H$_2$O in aqueous carbonate solutions. We performed a dissolution experiment and considered the effect of CO$_3^{2-}$ coordination and hydration in a real solution using MD simulation. Then, we performed DFT quantum chemistry calculations, UV-vis spectral analysis, inversion, and in-depth analysis [Y(CO$_3$)$_m$·nH$_2$O]$_{1-2m}$ of the morphology and ionic structure of Y to clarify its evolution mechanism in carbonate solution. The results of this work could explain the problem of rare-earth yield in ionic rare-earth precipitation.

2. Experimental materials and research methods

2.1 Experimental materials and equipment

The raw materials used in this experiment were obtained from a high-purity YCl$_3$ solution produced by a rare-earth separation plant in Longnan county, Ganzhou. The main component of the YCl$_3$ solution was prepared by oxalic acid precipitation, burning, HCl dissolution, and determined by ICP-MS and are shown in Table 1. Other chemical reagents used, such as Na$_2$CO$_3$ and H$_2$O, were of analytical purity. The experimental equipment or instruments used in this work are shown in Table 2.

2.2 Research method

2.2.1 Instantaneous saturated dissolution of Y$^{(n)}$. The calibrated YCl$_3$ solution was added dropwise to a series of 50 mL solutions containing 0.4, 0.8, 1.2, 1.6, or 2.0 mol L$^{-1}$ Na$_2$CO$_3$, keeping in a conical flask at 35 °C under water-bath conditions. The conical flask was then removed from the water bath and shaken. After drop-wise addition of the YCl$_3$ solution to the carbonate solutions, a white precipitate was produced. As the conical flask oscillated, the white precipitate dissolved. Addition of the rare-earth liquid was continued until dissolution of the white precipitate could no longer be completed. Next, the solution was centrifuged for 10 min at 35 ± 1°C and 9000 rpm. The supernatant was titrated with EDTA to determine the molar concentration of Y$^{(n)}$, which was defined as the instantaneous saturated dissolution amount of Y$^{(n)}$. The instantaneous saturated molar concentrations of Y$^{(n)}$ in different concentrations of Na$_2$CO$_3$ solution was calculated at 35 ± 1°C.

2.2.2 Molecular dynamics calculations. Molecular Dynamics (MD) is a method of analyzing the movement of ions or molecules in a system from the microscopic level; here, theoretical simulation of various characteristics of the system is achieved through correlation calculation of statistical mechanics.

For the microscopic behavior of Y element in carbonate solution system, according to the instantaneous saturated solution of Y$^{(n)}$ in different concentrations of Na$_2$CO$_3$ solution, the SPC/E water model used was used to calculate the MD of its real solution system. The radial distribution function (RDF) and coordination number of each ion pair in the carbonate solution system were calculated and analyzed, and the Y$^{(n)}$ coordination form considering CO$_3^{2-}$ was determined.

Geometric and energy optimization of Y$^{3+}$, Cl$^-$, H$_2$O, and CO$_3^{2-}$ contained in the solution system were achieved by using the Forceite module in the calculation platform Materials Studio 8.0. The initial simulation model was a cube system...
Table 1  Contents of each element and REE distribution in high purity YCl₃

| Y³⁺, mol L⁻¹ | H⁺, mol L⁻¹ | Density, g mL⁻¹ | Rare earth impurities/REO (µg mL⁻¹) |
|-------------|-------------|----------------|-------------------------------------|
| 0.3419      | <0.10       | 1.0568         | La₂O₃                                 |
|             |             |                | CeO₂                                 |
|             |             |                | Pr₆O₁₁                                |
|             |             |                | Nd₂O₃                                 |
|             |             |                | Sm₂O₃                                 |
|             |             |                | Eu₂O₃                                 |
|             |             |                | Gd₂O₃                                 |
|             |             |                | Tb₂O₃                                 |
|             |             |                | Dy₂O₃                                 |
|             |             |                | Ho₂O₃                                 |
|             |             |                | Er₂O₃                                 |
|             |             |                | Tm₂O₃                                 |
|             |             |                | Yb₂O₃                                 |
|             |             |                | Lu₂O₃                                 |

established by the Amorphous cell module in Materials Studio 8.0. The water molecules and ions were randomly distributed in the system. The universal force field was used, and the system was geometrically optimized by the Smart method. The parameters were preset in the operation, the calculation step was 1 fs, the total calculation time was 500 ps, the temperature control setting mode was set to Andersen, the system temperature was based on 308 K, and the NVT ensemble was selected. The accuracy of the simulation calculations was set to 0.3419 <0.10 1.0568 La₂O₃ CeO₂ Pr₆O₁₁ Nd₂O₃ Sm₂O₃ Eu₂O₃ Gd₂O₃

Table 2  Experimental equipment specification information table

| Equipment                                      | Type specification | Manufacturers                           |
|------------------------------------------------|--------------------|-----------------------------------------|
| High-speed centrifuge                          | TGL16MS            | Yancheng Anxin Experimental Instrument Co., Ltd. |
| Computer server                                | IBM System X3850 X5| International Business Machines Corporation |
| UV-visible spectrophotometer (UV-vis)           | UV-5500PC          | Shanghai yoke instrument Co., Ltd.       |
| Inductively coupled plasma-optical emission spectroscopy (ICP-OES) | ULTIMA2            | HORIBA Jobin Yvon                        |
| pH meter                                       | KL-009             | Xuzhou Yaming Instrument Co., Ltd.       |

2.2.4 DFT geometry optimization. Based on the chemical composition of the Y(III) complex ions obtained in the MD simulations, geometric optimization of the Y(III) complex ion structure and calculation of the characteristic UV absorption spectrum were performed by DFT. The DMol3 module in Materials Studio 8.0 was used for DFT computation. The GGA/PBE method was selected, and the base was set to DND 4.4. TD-DFT calculation was conducted using the COSMO solvation model. The integration precision, SCF tolerance, and track cutoff were set to fine. During MD simulations, the possible ion structures were obtained, geometric optimization and total energy calculation of the system were conducted, and excited-state UV spectra were calculated using the same basis set and method.

3. Results and discussion

3.1 Instantaneous saturated dissolution of Y(III)

The instantaneous saturated molar concentrations of Y(III) in 50 mL of 0.4, 0.8, 1.2, 1.6, and 2.0 mol L⁻¹ Na₂CO₃ solution at 35 °C are shown in Fig. 1.

The experiments confirm that the dissolution process of Y occurs in the Na₂CO₃ solution. A precipitate form when YCl₃ is added to the Na₂CO₃ solution, but this solid is dissolved as the reaction proceeds, thus leaving a clear solution. At this time, Y(III) in the solution does not precipitate as a rare-earth carbonate but is dissolved in the Na₂CO₃ solution. However, when the added amount of Y(III) exceeds the instantaneous saturated dissolved amount, the solution no longer clears; instead, it assumes the form of a suspension. In this case, part of Y(III) in the solution is precipitated; the amount of dissolved rare-earth ions when the flocculent turbidity is produced is considered the instantaneous saturated dissolved amount. Fig. 1 shows that the instantaneous saturated dissolved amounts of Y in 0.4, 0.8, 1.2, 1.6, and 2.0 mol L⁻¹ Na₂CO₃ solutions are 0.0041, 0.0163, 0.0377, 0.0693, and 0.0909 mol L⁻¹, respectively. The relationship between the
instantaneous saturated dissolved amount of Y and the concentration of CO$_3^{2-}$ in the base solution was analyzed, and Fig. 1 shows that the Y(III) instantaneous saturated dissolved amount has a linear relation with the concentration of CO$_3^{2-}$. The equation describing this relationship is 

$$y = 0.0416x + 0.0074,$$

and the $R^2$ is 0.985. This result provides a basis for designing a model of a real solution with different concentrations of CO$_3^{2-}$.

### 3.2 MD

#### 3.2.1 Radial distribution and coordination number.

Radial distribution function (RDF) analysis is conducted on the MD calculation results, and the RDF between the components in the system is associated with the coordination number. Eqn (2) is used to calculate the average coordination number between components. The definitions of $g(r)$ and $C_n$ are shown in Fig. 2.

The calculation formulas are as follows:

$$g(r) = \frac{V n(r, \Delta r)}{N 4\pi r^2 \Delta r}$$

$$C_n(r) = 4\pi \rho \int_0^r g(r')r'^2 dr'$$

where $V$ is the total volume of the system; $N$ is the total number of particles in the system; $n(r, \Delta r)$ is the number of particles from $r$ to $r + \Delta r$; $\rho$ is the bulk density (ratio of the number of particles to the bulk volume); $C_n(r)$ is the number of coordination atoms (molecules) in the range of $0$-$r$ spherical shell around the target atom; $\rho$ is the number density of the coordination atom (or molecular), that is, the ratio of the number of atoms (molecule) to the volume of space; $g(r)$ is the value of the radial distribution function, indicating the probability of occurrence of a coordinating atom (or molecular) within a certain distance; $r$ is the intercept radius.

Before the results are described and discussed, a representation the RDF for the studied simulation system should be
defined. O_{(i)} is an oxygen atom of carbonates in the first coordination shell of Y(III), and O_{(j)} is an oxygen atom farther away from Y(III) in the carbonates. In order to directly investigate the distribution of H_2O around Y(III), H_2O is considered a whole particle to analyze the RDF of H_2O for Y(III) and calculate the coordination number. After each solution simulation is performed and the MD simulations are converged, the RDF and coordination number of Y^{3+}–O, Y^{3+}–H_2O, and Y^{3+}–Cl^{-} are calculated separately. The simulation results are shown in Fig. 3–5.

Fig. 3–5 show the RDFs of Y^{3+} and O_{(i)}, O_{(j)} H_2O, and Cl^{-}; the RDF directly reflects the microscopic information of the ions in the rare-earth carbonate solution system. According to the figures (a, b2, c2, d2, e2, and f2), the average coordination of Y^{3+} and Cl^{-} has zero RDF intensity, and Y^{3+} and Cl^{-} coordination does not occur. These results indicate that the interaction of Y^{3+} with Cl^{-} in the solution may be negligible. The Y(III) short-range has two hydrated shells in the YCl_3–H_2O solution and the YCl_3–Na_2CO_3 solution system; in the central ion close-range ordered layer, RDF counts all ordered short-range particles. In existing research and literature, we can conclude that the interaction between CO_3^{2–} and Y(III) is reduced to 2.2, consistent with the conclusion reported by Martelli. In the high-CO_3^{2–}-concentration solution, the change in CO_3^{2–} concentration has nearly no effect on the peak position of the RDF; it affects the peak of g(r) only.

According to the specific simulation values in Table 4, we initially predict, the ionic composition of Y(III) in the YCl_3 solution is [Y:3H_2O]. Y(III) mainly exists in the form of a complex [YCO_3:3H_2O]^{37} in 0–0.8 mol L^{-1} CO_3^{2–} solution and in the form of a complex [Y(CO_3)_{2}:2H_2O] in 1.2–2.0 mol L^{-1} CO_3^{2–} solution. In the solution with high CO_3^{2–} concentration, H_2O in Y(III) short-range is crowded by the CO_3^{2–} space. In the first water molecule shell, the coordination number of H_2O for Y(III) is reduced to 2.2, consistent with the conclusion reported by Martelli. In the high-CO_3^{2–}-concentration solution, the hydration number of heavy rare-earth carbonate Ln(III) is 4–2. When CO_3^{2–} ≤ 0.8 mol L^{-1}, one CO_3^{2–} passes through the second shell of the H_2O molecules from the outer layer and then enters the first shell to coordinate with Y(III). At this point, the effect of H_2O molecule crowding is not noticeable. However, when CO_3^{2–} is further increased, the second CO_3^{2–} passes through the second H_2O ordered layer from the outer layer then and enters the first shell to coordinate with Y(III). Under this condition, short-range CO_3^{2–} space crowding results in a decrease of 1–2 H_2O molecules around the Y(III) short-range. This result indicates that the interaction between CO_3^{2–} and Y(III) is that CO_3^{2–} is originally due to electrostatic attraction at a distant location, passing through the second layer of H_2O molecules, and entering the inner shell. Then, a coordination bond with Y(III) occurs.
It is worth mentioning, carbonate not only complexes rare-earth ions but also precipitates with rare-earth ions in carbonate solutions. In the high concentration CO$_3^{2-}$/C$_0$ solution system of this paper, due to the higher CO$_3^{2-}$/C$_0$ ion strength, CO$_3^{2-}$/C$_0$ will be squeezed into the short-range. It has been reported that with the increase of CO$_3^{2-}$/C$_0$ concentration, in short-range of H$_2$O will replace 1–2, a CO$_3^{2-}$/C$_0$ replaces a H$_2$O molecule, resulting in increase the coordination number 1 because there is two O elements of CO$_3^{2-}$/C$_0$ coordinated with Y(III). In a certain sense, high concentration of CO$_3^{2-}$/C$_0$ seem to have interactions like counterions on CO$_3^{2-}$/C$_0$ coordination, related theory of counterions on the hydration structure of lanthanide ions can be used to study this problem.  

3.2.2 Coordination mode of CO$_3^{2-}$ for Y(III). The MD simulation results show the change trend of the average coordination number of H$_2$O and CO$_3^{2-}$/C$_0$ for Y(III), and the approximate evolution process of Y(III) complex ions is obtained. According to the simulation results of b, c, d, e, and f, two O atoms in the carbonate are arranged in the first shell, and the one remaining O atom is ordered in the second shell far away from Y(III), and their relative distance is stable. Considering the interaction distance of the coordination bond in the range of the overall chemical bond ($r < 2.6$ Å), we believe that two O$_{C(n)}$ atoms in the carbonate solution are combined with Y(III) in a coordinated manner. However, far away from Y(III), the O$_{C(f)}$ atom is combined with the C atom, the relative distance between $r_{Y-O_{C(n)}}$ and $r_{Y-O_{C(f)}}$ is also stable, and the characteristic peak positions of O$_{C(n)}$ and O$_{C(f)}$ are at a consistent ratio. According to the actual geometry of CO$_3^{2-}$, in the solution, CO$_3^{2-}$ takes the O$_{C(n)}$ atoms to the Y atom and combines with Y(III) via bidentate coordination.

In order to demonstrate CO$_3^{2-}$ for the Y(III) coordination mode, we assume that the coordination mode of each CO$_3^{2-}$ to Y atom is bidentate form, $r_{Y-O_{C(n)}}$ is the distance between the Y(III) short-range Y atom and the CO$_3^{2-}$ first-coordination-layer O atom, and $r_{Y-O_{C(f)}}$ is the distance between Y(III) and O$_{C(f)}$. The distance between the other atoms is defined as shown in Fig. 6. In these MD simulation studies, CO$_3^{2-}$ is a rigid particle, where $r_{C-O}$ and $r_{C=O}$ are 1.269 Å, $\angle COO = 120^\circ$ according to the principle of minimum energy, and $\angle YCO = 60^\circ$.

On the basis of these known conditions, we infer the relationship between $r_{Y-O_{C(n)}}$ and $r_{Y-O_{C(f)}}$ via the following reasoning:

$$x_1 = \sin 60^\circ r_{C-O}$$

(3)

$$x_2 = \cos 60^\circ r_{C-O}$$

(4)

$$x_3 = \sqrt{r_{Y-O_{C(n)}}^2 - x_1^2}$$

(5)

$$r_{Y-C} = x_2 + x_3$$

(6)

$$r_{Y-O_{C(n)}} = x_2 + x_3 + r_{C=O}$$

(7)

$$r_{Y-O_{C(f)}} = \cos 60^\circ r_{C-O} + \sqrt{r_{Y-O_{C(n)}}^2 - (\sin 60^\circ r_{C-O})^2} + r_{C=O}$$

(8)

![Fig. 4 RDF and coordination number of each ligand for Y(III) in YCl$_3$–H$_2$O solution system. (Model b: b1 and b2, Model c: c1 and c2.)](image)
By substituting the values of $r_{c-O}$ and $r_{c=O}$ to eqn (8), we calculate $r_{Y-O_{CO}}$.

$$r_{Y-O_{CO}}(n) = 1.9035 + \sqrt{r_{Y-O_{CO}}(n)^2 - 1.2078}$$  \hspace{1cm} (9)

According to the definition of Fig. 6, the following relationship can also be determined: $N_{O_{CO}} : N_{O_{CO}} = 2 : 1$.

$$N_{O_{CO}} = C_{nY-O}(r < 4.0 \text{ Å}) - C_{nY-O}(r < 4.0 \text{ Å})$$  \hspace{1cm} (10)

### Table 4  MD simulation calculation results

| Model | $r_{Y-O_{CO}}$ \(\text{Å}\) | $C_{nY-O}(r < 2.6 \text{ Å})$ | $r_{Y-O_{CO}}$ \(\text{Å}\) | $C_{nY-O}(r < 4.0 \text{ Å})$ | $N_{O_{CO}}$ | $N_{O_{CO}}$ | $N_{O_{CO}}/N_{O_{CO}}$ | $r_{Y-H_{2}O}$ \(\text{Å}\) | $C_{nY-H_{2}O}(r < 2.6 \text{ Å})$ |
|-------|----------------|------------------|----------------|------------------|-------------|-------------|-------------------|----------------|------------------|
| a     | —              | —                | —              | —                | —           | —           | —                 | 2.27           | 3.0              |
| b     | 2.15           | 2.0              | 3.75           | 3.0              | 2.0         | 1.0         | 2.0               | 2.35           | 3.0              |
| c     | 2.15           | 2.1              | 3.75           | 3.1              | 2.1         | 1.0         | 2.1               | 2.35           | 2.8              |
| d     | 2.15           | 4.0              | 3.75           | 6.0              | 4.0         | 2.0         | 2.0               | 2.37           | 2.6              |
| e     | 2.15           | 4.0              | 3.75           | 6.0              | 4.0         | 2.0         | 2.0               | 2.40           | 2.4              |
| f     | 2.25           | 4.1              | 3.75           | 6.1              | 4.1         | 2.0         | 2.0               | 2.40           | 2.2              |
According to the calculation results in Table 4, $N_{O_{(c)}} : N_{O_{(f)}}$ are all $2:1$ among models b, c, d, e, and f. The relationship between their $r_{Y-O_{(c)}}$ and $r_{Y-O_{(f)}}$ agrees well with eqn (9). Therefore, our assumptions are true. Regardless of CO$_3^{2-}$ concentration, CO$_4^{2-}$ and Y(III) are combined in the form of bidentate coordination. In Na$_2$CO$_3$ solution systems of different concentrations, only the Y(III) ion CO$_3^{2-}$'s average coordination number and hydration number change. With increasing CO$_3^{2-}$, the coordination number of the O atom to Y(III) changes. The $O_{(c)}$ (n) atoms are directly coordinated with Y(n), that is, $CN_{Y-O} (r < 2.6 \text{ Å})$ is the average coordination number of O.$^{30}$ When CO$_3^{2-}$ concentration is 0.4–0.8 mol L$^{-1}$, the coordination number of O atom to Y(III) is 2, the coordination number of H$_2$O molecule to Y(III) is 3; while the concentration of CO$_3^{2-}$ is 1.2–2.0 mol L$^{-1}$, the coordination number of O atom to Y(III) is 4, and the coordination number of H$_2$O molecule to Y(III) is 2. Therefore, the total coordination number of Y(III) in YCl$_3$ aqueous solution is 3, and the total coordination number of Y(III) is 5 when CO$_3^{2-}$ concentration is 0.4–0.8 mol L$^{-1}$, and the total coordination number of Y(III) is 6 when the concentration of CO$_3^{2-}$ increases to 1.2–2.0 mol L$^{-1}$. In a high-concentration (CO$_3^{2-}$ > 1.2 mol L$^{-1}$) carbonate solution, Y(III) mainly exists in the bidentate coordination form of [Y(CO$_3$)$_2$·2H$_2$O]$^-$.$^{31}$ This finding is consistent with the conclusion by Jeanvoine$^{32}$ that the carbonate of Ln(III) in aqueous solution shows bidentate coordination.

### 3.3 UV-vis full wavelength scanning absorption spectroscopy

Before the results are analyzed and discussed further, the characteristics of some experimental results is explained. A$_0$, which is the UV-vis absorbance curve, is determined by adding 1 mL of YCl$_3$ to 25 mL of pure water. A$_{0.4}$, A$_{0.8}$, A$_{1.2}$, A$_{1.6}$, and A$_{2.0}$ are the UV-vis absorbance curves determined by adding 1 mL of YCl$_3$ to 25 mL solutions of 0.4, 0.8, 1.2, 1.6, and 2.0 mol L$^{-1}$ Na$_2$CO$_3$, respectively. After mixing, the mixture is centrifuged, and the supernatant is subjected to UV-vis full-wavelength scanning to obtain the corresponding UV-vis absorbance curves. B$_{0.4}$, B$_{0.8}$, B$_{1.2}$, B$_{1.6}$, and B$_{2.0}$ are the UV-vis absorbance curves determined by adding 1 mL of pure water to 25 mL solutions of 0.4, 0.8, 1.2, 1.6, and 2.0 mol L$^{-1}$ Na$_2$CO$_3$, respectively. After mixing, the UV-vis full-wavelength scanning absorption curve is measured by the same method as a blank control spectrum. The results of UV-vis full-wavelength scanning analysis are shown in Fig. 7.

Fig. 7(a0) illustrates that the UV-vis characteristic absorption peak of the YCl$_3$–H$_2$O solution system is $\lambda = 203$ nm. Fig. 7(b0 and c0) show the UV absorption peaks of the YCl$_3$–Na$_2$CO$_3$ solutions (0.4 and 0.8 mol L$^{-1}$ CO$_3^{2-}$) and the corresponding blank control spectrum. The characteristic absorption wavelengths of A$_{0.4}$ and B$_{0.4}$ is close, A$_{0.8}$ and B$_{0.8}$ is also close. But the absorbance of A$_{0.4}$ at $\lambda = 224$ nm is significantly stronger than that of B$_{0.4}$, and the absorbance of A$_{0.8}$ at $\lambda = 225$ nm is significantly stronger than B$_{0.8}$ at peak position. Fig. 7(d0, e0 and f0) show the UV absorption peaks of the YCl$_3$–Na$_2$CO$_3$ solutions (1.2, 1.6, and 2.0 mol L$^{-1}$ CO$_3^{2-}$) and the corresponding blank control spectrum. The UV-vis characteristic absorption peaks at $\lambda = 217$–218 nm for A$_{1.2}$, A$_{1.6}$, and A$_{2.0}$ and their peak absorbances are remarkably stronger than those of the corresponding B$_{1.2}$, B$_{1.6}$, and B$_{2.0}$ systems. The results of MD calculation should be verified via quantum chemical calculation to further analyze and demonstrate the Y(III) coordination morphology in the YCl$_3$–Na$_2$CO$_3$ solution systems of different CO$_3^{2-}$.

#### 3.4 DFT calculation results

**3.4.1 Ion structure and theoretical calculation UV spectroscopy**. Based on the complex ion composition obtained by the MD simulations and considering the first shell of Y(III) in the Y–carbonate complex solution system, we optimize the Y(III) complex structure and calculate the UV spectrum via the DFT method. Fig. 8 shows the quantum chemical calculation UV spectrum and optimized structure of [Y–3H$_2$O]$^{3+}$, [YCO$_3$–3H$_2$–O]$^-$, and [Y(CO$_3$)$_2$·2H$_2$O]$.^{33}$

In this section, the absorption curve measured by UV-vis full-wavelength scanning is obtained by adding 1 mL of YCl$_3$ to several Na$_2$CO$_3$ solutions; in fact, it is the overlap of the absorption curve generated by Y(III) complex ions [including [Y–3H$_2$O]$^{3+}$, [YCO$_3$–3H$_2$–O]$^-$, and [Y(CO$_3$)$_2$·2H$_2$O]$^-)] and the absorption bands of the solvent (Na$_2$CO$_3$, H$_2$O). Although the solvent itself has its own UV absorption band, the characteristic peak wavelength of the UV-vis full-wavelength scan of Fig. 7(a0) is close to the wavelength of the calculated UV spectral characteristic absorption of Fig. 8(S1). Moreover, the UV-vis characteristic absorption peaks at $\lambda = 217$–218 nm for A$_{1.2}$, A$_{1.6}$, and A$_{2.0}$ are significantly stronger than those for the corresponding B$_{1.2}$, B$_{1.6}$, and B$_{2.0}$ curves. This finding verifies that Y(III) exists in the form of [Y–3H$_2$O]$^{3+}$ in the YCl$_3$ aqueous solution. The peak positions of the UV-vis full-wavelength scans of Fig. 7(d0, e0 and f0) are consistent with the absorption peak position of the UV spectrum characteristic of Fig. 8(S3), that is, the theoretically calculated UV spectral absorption characteristic peak position and the experiment measured absorption peaks of the UV-vis full-wavelength scan are consistent. Thus, Y(III) is a 6-coordinated complex [Y(CO$_3$)$_2$·2H$_2$O]$^{-}$ in the 1.2–2.0 mol L$^{-1}$ Na$_2$CO$_3$ solution. In Fig. 7, the results of UV-vis full-wavelength scanning analysis of B$_{0.4}$, B$_{0.8}$, B$_{1.2}$, B$_{1.6}$, and B$_{2.0}$ show a certain absorption band in the blank control sample, which means the Na$_2$CO$_3$ solution itself presents some UV absorption, and the absorption curves of different concentrations of Na$_2$CO$_3$ solution are basically the same.
However, comparison between the UV test results of Fig. 7(b0 and c0) and the calculated spectra of Fig. 8(S2) shows that the absorption band of Na$_2$CO$_3$ solution considerably influences the absorption intensity and absorption peak wavelength of A0.4 and A0.8. That is, in the Na$_2$CO$_3$ solution with low CO$_3$$^{2-}$ concentration, the UV absorption band of the solvent itself greatly affects the peak position and absorption intensity of the UV absorption curve of [YCO$_3$$\cdot$3H$_2$O]$^+$. It can be seen from Fig. 8(S2) and Fig. 7(b0, c0), the characteristic absorption peak wavelength of [YCO$_3$$\cdot$3H$_2$O]$^+$ is $\lambda = 203.7$ nm, which is not seen in the experimental analysis of the low-CO$_3$$^{2-}$-concentration Na$_2$CO$_3$ solutions (in absorbance curve of A0.4 and A0.8), because the characteristic peak of the Y-O$_w$ bond at $\lambda = 203.7$ nm is not revealed in such solutions. The absorption bands B0.4 and B0.8 of the Na$_2$CO$_3$ solution itself are at a low absorption level of $\lambda = 203.7$ nm. Therefore, the UV spectrum
obtained by the experimental test (A0.4 and A0.8) is the result of superimposing the UV absorption band of \([\text{YCO}_3\cdot3\text{H}_2\text{O}]^+\) as the solute in the solution and the absorption band of the Na$_2$CO$_3$ solution.\(^{44}\) This process results in the theoretical UV absorption peak of \(\lambda = 203.7\) nm, which is not reflected in the experimental analysis of the UV spectrum. In Fig. 8(S2), the characteristic absorption band of \([\text{YCO}_3\cdot3\text{H}_2\text{O}]^+\) at \(\lambda = 220–240\) nm, which resembles a shoulder peak, is enhanced in the experimental UV spectrum.\(^{45}\) Thereby, the absorption band of \([\text{YCO}_3\cdot3\text{H}_2\text{O}]^+\) calculated UV spectrum (Fig. 8(S2)) at \(\lambda = 220–240\) nm, is exhibited in Fig. 7(b0, c0) at \(\lambda = 224–225\) nm.

We analyze the bond length information of Y(III) complex ions by DFT geometry optimization. The structural results of carbonate complex ion S1, S2, S3 complexes obtained from DFT calculation are shown in Table 5. Here, Y–O$_{\text{vic}}$ represents the distance between the Y atom and the nearer O atom in the carbonate, and Y–O$_W$ represents the distance between the Y atom and the O atom in the water molecule.

In the RDF analysis of the MD simulation, the first shell of the O atoms interacting with Y(III) and the first shell of H$_2$O are analyzed, that is, Y(III) and each ligand the distance between them. Comparison of the values in Tables 4 and 5 shows that in model a, \(r_{Y-H_2O}\) is close to the value of Y–O$_W$ in models b and c, \(r_{Y-CO_3(n)}\) and the values of Y–O$_{\text{vic}}$ are consistent, and \(r_{Y-H_2O}\) is close to the value of Y–O$_{\text{vic}}$ in models d, e, and f, \(r_{Y-H_2O}\) is close to the value of Y–O$_{\text{vic}}$, and the values of \(r_{Y-H_2O}\) and Y–O$_W$ are close. The comparison also shows that the coordination around Y(III) is CO$_3^{2–}$. When the coordination number of CO$_3^{2–}$ is increased from 1 to 2, the length of Y–O$_W$ in the first shell of the H$_2$O molecule increases. Therefore, the distance between Y(III) and O$_{\text{vic}}$ obtained by MD simulation is consistent with the bond length Y–O$_{\text{vic}}$ calculated by DFT. The distance \(r_{Y-H_2O}\) of the first shell of the H$_2$O molecule is also consistent with the bond length of Y–O$_W$ calculated by DFT. In summary, the DFT calculation results and the experimental UV-vis analysis are well-validated by the MD simulation results.

According to the results of the MD simulation, dissolve experiment and UV-vis full-wavelength scanning experiment, three complex ions of Y(III) can be gradually transformed into each other increases with the concentration of CO$_3^{2–}$ increasing, the process of which is shown in Fig. 9.

With increasing of the CO$_3^{2–}$ concentration, the following dynamic balance exists in the YCl$_3$–Na$_2$CO$_3$ solution system:

$$\text{YCl}_3 \rightleftharpoons \text{Y}^{3+} + 3\text{Cl}^- \quad (11)$$

$$\text{Y}^{3+} + 3\text{H}_2\text{O} \rightleftharpoons [\text{Y}\cdot3\text{H}_2\text{O}]^{3+} \quad (12)$$

$$[\text{Y}\cdot3\text{H}_2\text{O}]^{3+} + \text{CO}_3^{2–} \rightleftharpoons [\text{YCO}_3\cdot3\text{H}_2\text{O}]^+ \quad (13)$$

$$[\text{YCO}_3\cdot3\text{H}_2\text{O}]^+ + \text{CO}_3^{2–} \rightleftharpoons [\text{Y(CO}_3)_{2}\cdot2\text{H}_2\text{O}]^- + \text{H}_2\text{O} \quad (14)$$

Fig. 9 illustrates that for \([\text{Y}\cdot3\text{H}_2\text{O}]^{3+}\) has one coordination point, with the concentration of CO$_3^{2–}$ increasing, preferentially combines one CO$_3^{2–}$ at the coordination point of \([\text{Y}\cdot3\text{H}_2\text{O}]^{3+}\), and converts to \([\text{YCO}_3\cdot3\text{H}_2\text{O}]^+\) complex ions, while the concentration of CO$_3^{2–}$ further increase, there will be a second CO$_3^{2–}$ to replace one of the H$_2$O molecules in the first shell, as in the reaction of (14) process, \([\text{YCO}_3\cdot3\text{H}_2\text{O}]^+\) transforms to \([\text{Y(CO}_3)_{2}\cdot2\text{H}_2\text{O}]^-\). Under different CO$_3^{2–}$ concentration

Table 5 Structural results for S1, S2, S3 complexes in bulk water obtained from DFT calculations

| Structure | Complex ion composition | Y–O$_{\text{vic}}$ (Å) | Y–O$_W$ (Å) |
|-----------|------------------------|------------------------|--------------|
| S1        | \([\text{Y}\cdot3\text{H}_2\text{O}]^{3+}\) | —                      | 2.24         |
| S2        | \([\text{YCO}_3\cdot3\text{H}_2\text{O}]^+\) | 2.17                   | 2.32         |
| S3        | \([\text{Y(CO}_3)_{2}\cdot2\text{H}_2\text{O}]^-\) | 2.25                   | 2.43         |
of the YCl₃–Na₂CO₃ solution system, the complex ion morphology of [Y(III)] is consistent with the conclusion reported by Jeanvoine. This result is also in line with Philippini’s conclusion that Ln(III) coordinates with additional CO₃²⁻ ions with increasing concentration of CO₃²⁻.

In our analysis of the instantaneous saturated dissolution of Y(III) in Na₂CO₃ solution, we believe that, given the coordination effect of a high concentration of CO₃²⁻ ions on Y(III) along with the CO₃²⁻ concentration increase, reaction eqn (13) and (14) are promoted in the positive direction, thereby increasing the instantaneous saturated solubility of Y(III). Therefore, according to the Y(III) dissolution experiment results, MD simulation studies of different concentrations of the YCl₃–Na₂CO₃ real solution system are performed. By combining the DFT calculation results and experimental UV-vis analysis, we can accurately resolve the microstructure and behavior of CO₃²⁻ coordination and hydration for Y(III). We reveal that the large mother liquor ion loss in rare-earth carbonate precipitation is caused by CO₃²⁻ coordination and hydration; consequently, REE is dissolved in the carbonate solution in the form of complex ions, resulting in incomplete precipitation of rare-earth.²⁶

4. Conclusions

In this study, a Y(III) dissolution experiment in Na₂CO₃ solution was used to determine the instantaneous saturated solubility of Y(III) in Na₂CO₃ solution, and the macroscopic dissolution law of Y(III) with CO₃²⁻ concentration was obtained. The RDF and coordination number of Y(III) by CO₃²⁻ and H₂O were systematically analyzed using MD simulations to obtain the complex ion form of Y(III) in carbonate solution. DFT was adopted to geometrically optimize and calculate the UV spectrum of the Y(III) complex ions. Findings are then compared with the experimentally determined UV-vis spectra and analyzed to further verify the reliability of the MD simulation results. The main conclusions are as follows.

(1) YCl₃ is added to Na₂CO₃ solution with instantaneous saturated dissolution, and a coordination effect on Y(III) is observed. The higher the CO₃²⁻ concentration, the easier the conversion to [Y(CO₃)₂·2H₂O]⁺ and the higher the instantaneous saturation dissolution of Y(III). When the initial concentration of Na₂CO₃ is 2 M, the instantaneous saturated dissolution of Y(III) in the carbonate reaches 0.0909 mol L⁻¹.

(2) In the aqueous solution of YCl₃, Y(III) exists in the form of [Y·3H₂O]³⁺. Each CO₃²⁻ with O atoms is close to the Y atom and combines via bidentate coordination. In 0–0.8 mol L⁻¹ CO₃²⁻ aqueous solutions, Y(III) is mainly 5-coordinated [YCO₃₂·3H₂O]⁺; with increasing CO₃²⁻ concentration, [YCO₃·3H₂O]⁺ is converted into 6-coordinated [Y(CO₃)₂·2H₂O]⁺.

(3) When Y(III) is added to aqueous solutions, hydrated [Y·3H₂O]³⁺ ions are preferentially formed, and [Y·3H₂O]¹⁺ exists as a coordination point. When CO₃²⁻ ≤ 0.8 mol L⁻¹, one CO₃²⁻ passes through the second shell of the H₂O molecules from the outer layer and enters the first shell to coordinate with Y(III). In this case, the effect of H₂O molecule crowding is not noticeable. As CO₃²⁻ is further increased, the second CO₃²⁻ passes through the second shell and enters the first shell of Y(III), thereby replacing one of three hydrated H₂O molecules in the form of a substitution reaction and initiating a bidentate coordination bond with Y(III). In this case, short-range CO₃²⁻ space crowding causes the H₂O molecule number around the short range of Y(III) to be reduced by 1–2.

Conflicts of interest

There are no conflicts to declare.

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