FROM ENGINE TO AFTERGLOW: COLLAPSARS NATURALLY PRODUCE TOP-HEAVY JETS AND EARLY-TIME PLATEAUS IN GAMMA RAY BURST AFTERGLOWS

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ABSTRACT

We demonstrate that the steep decay and long plateau in the early phases of gamma-ray burst X-ray afterglows are naturally produced in the collapsar model, by a means ultimately related to the dynamics of relativistic jet propagation through a massive star. We present two-dimensional axisymmetric hydrodynamical simulations that start from a collapsar engine and evolve all the way through the late afterglow phase. The resultant outflow includes a jet core that is highly relativistic after breaking out of the star, but becomes baryon loaded after colliding with a massive outer shell, corresponding to mass from the stellar atmosphere of the progenitor star which became trapped in front of the jet core at breakout. The prompt emission produced before or during this collision would then have the signature of a high Lorentz factor jet, but the afterglow is produced by the amalgamated post-collision ejecta that has more inertia than the original highly relativistic jet core and thus has a delayed deceleration. This naturally explains the early light curve behavior discovered by Swift, including a steep decay and a long plateau, without invoking late-time energy injection from the central engine. The numerical simulation is performed continuously from engine to afterglow, covering a dynamic range of over 10 orders of magnitude in radius. Light curves calculated from the numerical output demonstrate that this mechanism reproduces basic features seen in early afterglow data. Initial steep decays are produced by internal shocks, and the plateau corresponds to the coasting phase of the outflow.

Key words: gamma-ray burst: general – hydrodynamics – ISM: jets and outflows – relativistic processes – shock waves

1. INTRODUCTION

Possibly the most important result of Swift observations is the discovery of early-time plateaus in gamma-ray burst (GRB) afterglows (Gehrels et al. 2004; Granot 2007). There have been many scenarios invoked to explain this plateau. One explanation requires late-time energy injection from the GRB central engine (Nousek et al. 2006; van Eerten 2014; Zhang et al. 2006). Another proposition is that the radiation is produced in a long-lived reverse shock (Genet et al. 2007; Uhm & Beloborodov 2007). Other ideas include evolving microphysics (Granot et al. 2006a; Paizis et al. 2006) or a slow energy transfer from ejecta to the circumburst medium (Granot & Kumar 2006; Nousek et al. 2006; Kobayashi & Zhang 2007). It has also been suggested that viewing-angle effects may be significant (Eichler & Granot 2006; Granot 2007). Another possibility is that the plateau corresponds to the time before the deceleration phase of the afterglow (Lei et al. 2011; Shen & Matzner 2012), however this requires very modest Lorentz factors $\gamma \sim 30$. Other popular jet models which attempt to explain afterglow plateaus are two-component jet models (Ramirez-Ruiz et al. 2002; Berger et al. 2003; Peng et al. 2005; Granot et al. 2006a; Filgas et al. 2011). The usual idea of two-component flows assumes that the afterglow is a combination of emission from a narrow highly relativistic jet core and a wide, less relativistic envelope.

In this work, the goal is not to propose a given jet model and calculate the resultant light curve. Rather, a numerical calculation is performed starting from a collapsar engine (Woosley 1993; MacFadyen & Woosley 1999; MacFadyen et al. 2001) and evolving through the late afterglow phases, to determine what outflows naturally look like, and what sort of light curves are generically produced. The major discovery of this work is that light curves broadly similar to those discovered by Swift are naturally produced without any special ingredients, other than a collapsar which initially collimates the flow.

The outflow produced by the collapsar is not a standard two-component jet, but a “top-heavy” jet, which has radial as well as angular variation. In this case, a highly relativistic jet core is preceded by a heavy, baryon-loaded outer shell to the jet. The shell is massive enough to decelerate the entire jet core significantly upon collision. This collision produces internal shocks which will produce synchrotron emission, and the final result of the collision is a less relativistic amalgamated jet, which is responsible for the afterglow emission (see Figure 1).

The main goals of this study are to demonstrate that such a top-heavy jet is a natural outcome of a collapsar GRB engine, and that this top-heavy flow naturally produces the basic features of the early afterglow light curves, including long plateaus. The jet core consists of the relativistic material ejected from the engine after the jet has tunneled through the stellar interior. The heavy outer shell of the jet consists of material from the progenitor atmosphere which was originally in front of the jet head at breakout.

All of this is demonstrated numerically, in the first multi-dimensional numerical GRB study that evolves the entire burst, from engine to afterglow. This covers a dynamic range of over ten orders of magnitude in length scale. To date, such a range of scales has only been numerically resolved in one-dimensional studies, e.g., Kobayashi et al. (1999).
2. NUMERICAL SET-UP

The system is assumed to be governed by the equations of relativistic hydrodynamics,

\[
\partial_t (\rho u^\mu) = S_D
\]

\[
\partial_t (\rho (\epsilon + P) u^\mu + Pu^\mu) = S^\mu
\]

where \( \rho \) is proper density, \( P \) is pressure, \( \epsilon \) is the internal energy density, and \( u^\mu \) is the four-velocity. The equations are solved in two dimensions assuming axisymmetry. Magnetic fields have also been ignored in this calculation, so that this is a purely hydrodynamical jet model. The source terms \( S_D \) and \( S^\mu \) model the engine, which injects mass, energy and momentum into the system at small scales. An adiabatic equation of state is employed,

\[
P = (\gamma - 1) \epsilon
\]

with adiabatic index \( \gamma = 4/3 \), and relativistic units are chosen such that \( c = 1 \).

The hydrodynamical evolution is carried out using the JET code (Duffell & MacFadyen 2011, 2013, 2014), a moving-mesh technique tailored to radial outflows. This numerical method is particularly important for this problem, both because of the high Lorentz factors \( \gamma \sim 100 \) which must be fully resolved, and the tremendous range of length scales covered. In particular, the inner and outer boundaries are moved during the calculation, so that it is possible to evolve the jet over many orders of magnitude in radius, while only resolving a single order of magnitude at any one time.

2.1. Initial Conditions

The initial set-up is designed to model a jet breaking out of a Wolf–Rayet star. The initial data for this star was acquired using the MESA code (Paxton et al. 2011, 2013) to evolve a stellar model until just before core collapse. This provides density as a function of radius that will affect the dynamics of the jet and cocoon as the jet tunnels its way through the star. The initial stellar model assumes a low-metallicity rapidly rotating star, with an initial mass of 30 \( M_\odot \) and rotating at 99% of breakup velocity. The star exhibits significant mass loss during its evolution, and the final state of the star before collapse is a Wolf–Rayet star with a mass of 18 \( M_\odot \) and about half the radius of the Sun. The choice of rotation velocity affects the initial mass and radius of the progenitor, but it was chosen assuming that a rapidly rotating progenitor may be necessary for jet production. In order to provide a standardized stellar model, a fitting function is used to approximate the result of the MESA output. The density as a function of radius is well-fit by the following:

\[
\rho(r,0) = \frac{\rho_q \left( \max(1 - r/R_\text{S}, 0) \right)^\gamma}{1 + \left( r/R_1 \right)^{\delta_1} / \left( 1 + \left( r/R_2 \right)^{\delta_2} \right)} + \rho_{\text{wind}} \left( r/R_3 \right)^{-2}.
\]

All of these parameters are listed in Table 1. The fitting function and MESA output are shown in Figure 2. Note that outside the stellar radius, the density has a wind profile \( \rho(r) = A/r^2 \), where \( A = \rho_{\text{wind}} R_3^2 = 1.2 \times 10^{13} \text{ g cm}^{-1} \approx 24 \).
times the typically assumed value of $5 \times 10^{11}$ g cm$^{-3}$, which assumes a wind velocity of 1000 km s$^{-1}$ and a mass-loss rate of $10^{-5} M_\odot$ yr$^{-1}$. The density surrounding the progenitor at death is not well known, and a factor of 24 above this fiducial value is not outside of the range of reasonable values for this constant. Velocity and pressure are initially set to negligible values:

$$v(r, 0) = 0,$$
$$P(r, 0) = 10^{-6} \rho(r, 0).$$

Of course, the injected jet will quickly raise these to non-negligible values in its vicinity. Gravity is not included in this calculation due to the short engine timescale considered; all of the dynamics are caused by the injection of energy and momentum at small radii.

2.2. Engine Model

The jet is injected deep within the stellar interior. The true engine operates on unresolved scales and consists of poorly understood physics. In the current study, the engine will be injected on resolved scales using a parameterized model. This is accomplished by the use of source terms in the hydrodynamical Equations (1) and (2). The engine is parameterized by a power, Lorentz factor, baryon loading, injection angle, injection radius, and engine duration (see Table 1).

The source terms are expressed in terms of the nozzle function, $g(r, \theta)$:

$$g(r, \theta) \equiv \left( r / n_0 \right) e^{-\left( r / n_0 \right)^2} \frac{e^{(\cos \theta - 1)} / \theta_0^2}{N_0}$$

where $N_0$ is the normalization of $g$:

$$N_0 \equiv 4 \pi n_0^3 \left( 1 - e^{-2 / \theta_0^2} \right) \theta_0^2$$

The source terms in Equations (1) and (2) are given by the following:

$$S^0 = L_0 e^{-t / \tau_0} g(r, \theta),$$
$$S^r = S^0 \sqrt{1 - 1 / \gamma_0^2}.$$

### Table 2

| Variable      | Definition                        | Value          |
|---------------|-----------------------------------|----------------|
| $\nu_{\text{obs}}$ | Observed Frequency                | $2.4 \times 10^{18}$ Hz |
| $\tau_b$     | Magnetic Energy Fraction          | 0.01           |
| $\epsilon_e$ | Electron Energy Fraction          | 0.1            |
| $p$          | Synchrotron Power Spectrum Slope  | 2.5            |
| $d_l$        | Luminosity Distance               | $5.5 \times 10^{28}$ cm |
| $\varepsilon$| Redshift                          | 2.2            |

$$S_D = S^0 / \eta_0.$$  \hspace{1cm} (11)

The parameters in the above equations for the source terms are all listed in Table 1. Engine power and duration are taken as typical values inferred from observations. The rest of the engine parameters are somewhat unconstrained, so the parameters are chosen so as to produce a reasonably collimated relativistic outflow. This model has many free parameters which could be varied to produce different jet properties. This has been done, for example, by MacFadyen et al. (2001), Zhang et al. (2003, 2004), and Morsony et al. (2007). It should also be noted that most jet breakout calculations use a “nozzle” boundary condition instead of a source term to model the engine. Either way this models unresolved physics, but the source-term method appears to produce more numerically stable outflows. As mentioned above, the injection radius $r_0$ is much larger than the true engine. This was done so as to ensure good resolution of the engine, which is covered by hundreds of computational zones, $\eta_0 / \Delta \tau_{\text{max}} \sim 10^2$. The size of the engine may impact the flow ejected from the progenitor.

2.3. Afterglow Light Curves

A synchrotron emission model is used to construct an afterglow light curve from the hydrodynamical output. The model is based on the one employed in van Eerten et al. (2010), though it is simplified in that it assumes the flow is optically thin. Electron cooling is accounted for using a global cooling timescale. The jet is also assumed to point directly at the observer. The synchrotron model parameters are summarized in Table 2. Note that this synchrotron model is designed for X-ray afterglows, and is less reliable in lower-frequency bands due to the global cooling timescale. All current results are presented in the X-ray, and multi-band studies are left for a future investigation that will employ a more complete synchrotron model.

3. RESULTS

Figures 3 and 4 show several stages in the evolution of the jet. First the engine drills out a tunnel in the stellar interior, supported by the hot cocoon surrounding it. The jet eventually breaks out of the star, producing a top-heavy outflow. The outer shell breaks out with a modest Lorentz factor ($\gamma_{\text{shell}} \sim 10$), in front of a highly relativistic ($\gamma_{\text{core}} \sim 100$) jet core. The thickness of this shell can be measured using data from the upper center panel of Figure 3. The thickness is calculated to be $\sim 10^{10}$ cm; analytic calculations of Waxman & Mészáros (2003) would predict a cork thickness of the order of $\theta R_5 \sim 5 \times 10^9$ cm, in rough agreement with our results. Because the material is all moving at nearly the same speed ($c$), the jet core does not collide with the shell until it has
expanded by several orders of magnitude ($t \sim \Delta r_{\text{shell}} \gamma_{\text{shell}}^2$).

When the core and shell collide, internal shocks are produced, and the two components of the jet merge to a single jet with modest Lorentz factor ($\Gamma \sim 30$). This process ends when the entirety of the jet core is absorbed, at $t \sim \Gamma \sim 30$. Internal shocks are therefore produced until the outflow has expanded to a radius of roughly

$$R_{\text{internal shocks}} \sim 10^{15} \text{ cm} \left( \frac{\gamma_{\text{shell}}}{30} \right) \left( \frac{\Gamma}{30} \right)^2$$

This radius of $10^{15}$ cm can be seen directly in Figure 5, as the transition from colliding to coasting occurs at $t \sim 3 \times 10^4$ s, when the flow has expanded to a radius of $ct \sim 10^{15}$ cm. This merged jet has more inertia than the original jet core, and so it decelerates at a later time than it would at the larger Lorentz factor $\gamma \sim 100$. Before this late deceleration time, there is a long coasting phase while the jet sweeps up a negligible amount of mass from the external medium. This translates into a long plateau in the afterglow light curve.

Figure 3 shows the evolution of the jet from the engine deep in the interior of the star to breakout from the star to the collimated outflow which produces afterglow emission. Overall, the calculation spans over 10 orders of magnitude in radius. The left half of each panel displays the logarithm of density, and the right half is the logarithm of the Lorentz factor. The large panel on the right is a snapshot at $t = 300$ s, shown in linear scale so that the massive shell is much more prominently displayed. In the top center and top right small panels ($t = 4.2$ s and $t = 12$ s), the thick dashed cyan curves indicate the surface of the progenitor, showing clearly that the jet breaks out before the engine turns off at $t = 10$ s.

Figure 5 shows Lorentz factor as a function of time, measuring Lorentz factor in two different ways. “Maximum Lorentz factor” $\gamma_{\text{max}}$ probes the fastest-moving material. Before the collision, this probes the jet core, whereas post-collision $\gamma_{\text{max}}$ probes the amalgamated jet. “Average Lorentz Factor” is weighted by energy, and essentially probes the average of the two components combined together. Thus, there is only a modest change in $\gamma_{\text{avg}}$ during the internal collisions, as the two flows amalgamate.

The light curve is shown in Figure 6. Indicated in this figure are the various stages in the evolution of the jet. The collision of the core with the outer shell produces internal shocks that give rise to a flare, which can last until observer time $t_{\text{obs}} \sim 100$ seconds. After this time there is a very steep decay, followed by a long plateau over several orders of magnitude. During this time the jet is massive enough that it is not forced to decelerate by the surrounding medium; this is the “coasting phase” of the jet. A forward shock is present ahead of the flow at this time, but its presence is not significant enough to affect the evolution of the jet until enough mass has been swept up, at the late deceleration time $t_{\text{obs}} \sim 10^{4-5}$ s. After this time, the jet begins...
to decelerate and the light curve begins to exhibit a power-law dependence consistent with the Blandford–McKee solution (Blandford & McKee 1976; Sari et al. 1998).

Also included in Figure 6 is Swift X-Ray data from GRB 110312 A (Evans & Oates 2011; Oates et al. 2011). The redshift of this burst is not known and is therefore treated as a free parameter. The plateau phase is reasonably modeled by the coasting, \( \Gamma \sim 30 \) jet, as is the late deceleration phase (consistent with the Blandford–McKee solution in a wind circumburst medium). The break times in this burst also coincide reasonably well with the numerical model in this work. However, in this instance they are about a factor of two later than those in the considered progenitor model. This suggests that this burst would be better fit by larger progenitors and longer-duration jets.

### 3.1. Improving the Fit to Data

It has clearly been demonstrated so far that the general shape of the light curve agrees with an example afterglow dataset (top two panels of Figure 6). This example was chosen partially because it is well sampled, and partially because it fit well with the acquired light curve for these parameters, but it should be emphasized that most early afterglows exhibit this same...
characteristic structure. It should also be emphasized that this required no special ingredients; the set of parameters of the progenitor star and engine was chosen at the beginning based on reasonable estimates, and therefore this result might be generic, as it did not require detailed tuning to achieve.

On the other hand, it is straightforward to use the inherent scale invariance of the fluid equations to find a better fit to the data (van Eerten & MacFadyen 2012; see also Granot 2012). The bottom panel in Figure 6 shows an afterglow constructed from the same numerical solution, but now assuming $R_0 = 2.3 \times 10^{11}$ cm. For example, the progenitor radius is $R_\text{f} \approx 2 R_0$ and the engine duration is $t_\text{f} = 33$ s (The energy of the burst and mass of the progenitor are still the same, as $M_0$ has not been rescaled). Not only does this provide a better fit to the data, but encouragingly this is a first step toward learning about the nature of the progenitor from the early stages of the afterglow light curve, by adjusting model parameters to fit the data. A more comprehensive study would vary all model parameters to find a fit; for now we vary only the parameter $R_0$ as this is easy to do (without performing additional numerical runs) using the scale invariance of the fluid equations. Future studies may be able to match afterglow data to model parameters by varying all of these parameters explicitly.

4. DISCUSSION

This work has demonstrated the following: first, that GRB afterglow plateaus are consistent with the coating phase of a low Lorentz factor jet, and second that such a jet naturally arises in a collapsar scenario due to the amalgamation of the highly relativistic jet core with a baryon-loaded outer shell. Additionally, this work demonstrates that internal shocks between the core and outer shell naturally produce the steep decay found at early times.

The details of this result are strongly dependent on the massive shell in front of the jet. During the time the jet is propagating through the star, there is a “jet head” that is not trapped in front of the engine, but can be pushed aside. However, as the jet accelerates and breaks out, there is a certain amount of material which becomes trapped in front of the jet (Waxman & Mészáros 2003). The amount of material trapped in the shell is difficult to precisely calculate even numerically; in fact it is found to be less pronounced in three-dimensional (3D) studies than in two-dimensional ones (Zhang et al. 2004). This shell’s properties will depend significantly on engine and progenitor properties, and on 3D and MHD effects. This dependence has been explored numerically in simulations of jet propagation through a stellar envelope (MacFadyen et al. 2001; Zhang et al. 2003, 2004; Morsony et al. 2007). Such an outer shell has also been referred to a “cork” and suggested as source of precursor emission (Waxman & Mészáros 2003) and as a “breakout shell” and suggested as a facilitator of prompt emission (Thompson 2006). The idea that this shell might decelerate the jet was also suggested by Shen & Matzner (2012). A similar idea was proposed to explain the radio afterglow of the giant flare from SGR1806-20 (Granot et al. 2006b). This explanation for afterglow plateaus has a large number of important consequences.

4.1. Requirement of Wind near Progenitors

If the plateau phase is described by a small negative slope, this requires that the external density profile during this phase be consistent with a stellar wind, \( \rho(r) \propto r^{-2} \). The slope of the afterglow during this phase can be calculated straightforwardly (e.g., Granot 2005; Shen & Matzner 2012). During this time the ejecta pushes a forward shock ahead of it, one that is too weak to decelerate the ejecta, but still powerful enough to produce significant synchrotron radiation. The scaling of the light curve can be calculated by modeling the system as a piston with constant Lorentz factor \( \Gamma \) pushing a shock ahead of it at this same Lorentz factor. Since \( \Gamma \) is fixed, it can be ignored in the scaling arguments. The shock jump conditions give

\[
P_{\text{shock}} \propto \rho_{\text{ext}}(r), \quad P_{\text{shock}} \propto \rho_{\text{ext}}^{\frac{3}{2}}(r),
\]

where \( \rho_{\text{ext}}(r) \propto r^{-k} \), with \( k = 2 \) for a wind. Assuming high frequencies in the slow cooling regime \( \nu_m \ll \nu_c < \nu \) (which is true in the external shocks of the numerical model presented here), then the flux is proportional to the volume of the emitting region \((\times r^3)\) and the emissivity \((\rho B \propto \rho^{\frac{3}{2}})^2\), and will also depend on the characteristic spectral break frequencies \( \nu_m \) and \( \nu_c \) (see for example van Eerten et al. 2010):

\[
F \propto r^3 \rho_{\text{ext}}^{\frac{3}{2}} \nu_m^{-1/2} \nu_c^{-1/2},
\]

where

\[
\nu_m \propto \rho_{\text{ext}}^{1/2}, \quad \nu_c \propto \rho_{\text{ext}}^{-3/2} t^{-2}, \quad r \propto t.
\]

The flux as a function of time is therefore

\[
F \propto \rho_{\text{ext}}^{3/2} t^{-2.5} \propto r^{-2} \propto t^{-2}.\]

The shape of the plateau in this model is then \( t^{-\alpha_x} \), where \( \alpha_x = -2 + k(p + 2)/4 \). For \( k = 2 \), \( \alpha_x = -p/2 \), which is always shallow and decaying for reasonable values of \( p \). For \( k = 2 \) and \( p = 2.5 \), this gives \( \alpha_x = 1/4 \) (This slope is shown in Figure 6). It is also straightforward to see from this that a negative slope favors \( k = 2 \). (For example, a uniform external density profile with \( k = 0 \) would always produce a rising afterglow slope, rather than a plateau.)

Thus, the environment within \( \sim 10^{16} \) cm of the progenitor must be a wind \((k \approx 2)\) in order for this model to make sense (though as mentioned in Section 2.1, the wind density in this study corresponds to \( A = A_0 \times (5 \times 10^{11} \text{ cm}^{-12}) \), where \( A_0 = 24 \), larger than typical inferred values). Additionally, the model predicts a particular slope to the spectrum, \( \nu^{-p/2} \). Analysis of these slopes in afterglow data has been carried out by Shen & Matzner (2012), who claim that a majority (55%) of bursts are consistent with this model.

4.2. Prediction of Steeper Slopes at Lower Frequencies

Optical observations of afterglow plateaus have found steeper slopes, with \( \alpha_{op} \) closer to unity. This is consistent with the coating model; if the frequency is below the cooling break, \( \nu_m < \nu_c < \nu \), then it is straightforward to show that \( \alpha_{op} \approx -3 + k(p + 5)/4 \). For \( k = 2 \), this gives \( \alpha_{op} = (p - 1)/2 = 3/4 \) for \( p = 2.5 \). Independent of \( p \), one finds the relationship

\[
\Delta \alpha \equiv \alpha_{op} - \alpha_x = 3k/4 - 1 \approx 1/2.
\]

More precisely, this model predicts that \( \Delta \alpha \approx 1/2 \) or 0, depending on whether the optical band is below the cooling break. This prediction is in contrast with the \( \Delta \alpha = 1/4 \), 0 prediction for a decelerating blastwave (e.g., Sari et al. 1998).

Many afterglow light curves appear to be consistent with
contrast with modeling of GRB 990123, for example (Sari & Piran 1999a).

4.4. Very Steep Decay of Internal Shock Emission

The extremely steep decay at early times ($\sim t^{-8}$, seen in Figure 6) is difficult to explain for a relativistic flow, because any steep decay in emission will be smoothed by the different arrival times of photons coming from different angles. However, if the jet’s properties vary significantly with opening angle, it is possible that this effect is compensated for. The large rightmost panel of Figure 3 shows the jet core as it is about to collide with the outer shell. The shape of the jet core suggests that the vary last part of the core to collide will be a narrow tail at low latitude $\theta \ll \theta_j$. The very last part of the internal shock emission is then dominated by emission from $\theta \ll \theta_j$, so that photons from larger opening angles might not smooth the light curve significantly.

4.5. Measurement of the Electron Distribution

If one assumes that the density profile is in fact a wind ($k = 2$), this provides a means to measure $\rho$, the slope of the electron power spectrum in the shock. Choosing $k = 2$ gives $p = 2 + 2\alpha$. Many X-ray plateau slopes cluster around $\alpha \sim 0.2$, favoring values of $p \sim 2.4$. However, this is a highly simplified reading of the data. For example, it is assumed here that there is no time dependence to the shock microphysical parameters. The slopes are also time dependent, as the light curve transitions from one regime to another, and it is not clear where these slopes should be measured from in order to achieve a clear interpretation.

4.6. Measurement of the Lorentz Factor

The deceleration time in a wind is given by $t_{\text{decel}} \sim t_{\text{Sedov}}/\Gamma^2$. In observer time this is $t_{\text{obs}} \sim t_{\text{Sedov}}/\gamma^2$. (The Sedov time $t_{\text{Sedov}} \equiv E_{\text{iso}}/(\rho_{\text{wind}} R_3^2 c^3)$ is defined here to be the time when the Jet has swept up a rest mass comparable to its isotropic equivalent energy.) Typical GRB parameters ($E_{\text{iso}} \sim 10^{54}$ erg, $\rho_{\text{wind}} R_3^2 \sim 10^{13}$ g cm$^{-3}$) can give $t_{\text{Sedov}} \sim 10^{10}$ s, and the break occurs at $t_{\text{decel}} \sim 10^8$ s, which strongly constrains typical Lorentz factors during the coasting phase to be $\Gamma \sim 30$. Such strong constraints may be very powerful for fitting afterglow data with initial jet models.

The plateau duration can be estimated as

$$t_{\text{decel}}/t_{\text{shocks}} \sim (t_{\text{Sedov}}/\gamma_0)^{-1/4} \sim \frac{t_{\text{Sedov}}/10^{10} \text{s}}{\gamma_0/10} \left(\frac{100}{\Gamma}\right)^{1/4}.$$  \hspace{1cm} (18)

This is consistent with the current results, where the plateau persists over a few orders of magnitude, so that $t_{\text{decel}}/t_{\text{shocks}} \sim 100$.

This motivates numerical studies exploring the parameter space of coasting jets with modest Lorentz factors, which should enable good fits of these model parameters to afterglow data, analogous to what has already been carried out for decelerating initial jet models (Ryan et al. 2015; Zhang et al. 2014).
4.7. Measurement of the Progenitor Mass

If the Lorentz factor $\Gamma$ can be constrained by the deceleration break time, this has important implications for understanding progenitors; if the energy $E$ and Lorentz factor $\Gamma$ are known, then $M = E/\Gamma$ is the mass loaded into the jet from the cocoon. It is possible that this mass could help constrain the mass of the progenitor, possibly using analytical models for the jet and cocoon (e.g., Bromberg et al. 2011, 2014) to connect the stellar mass to the ejecta mass. Such models would need to be revised to include the emergence of this massive shell in front of the jet core.

Alternatively, this question could be explored numerically, by performing high-resolution three-dimensional calculations of jets breaking out of various stellar models like those of Zhang et al. (2004), to determine if there is any reliable relationship between ejecta mass and progenitor mass.

4.8. Implications for Prompt Emission

Internal shocks have long been a leading model for prompt emission, though they usually are thought to result from the collision of multiple highly relativistic shells. If the jet is top-heavy such that the shell in front is baryon loaded (as proposed here), this causes the collision to be much more violent, and should increase the efficiency of internal shocks substantially. However, this picture does not preclude other models for prompt emission. It is possible that the steep decay is produced by internal shocks, but that some other mechanism is responsible for the gamma-rays themselves. Internal shock models may have difficulty explaining the details of the variability in the prompt emission.

4.9. Implications for Short Bursts

Everything invoked here applies to the collapsar scenario (Woosley 1993; MacFadyen & Woosley 1999; MacFadyen et al. 2001), which is thought to describe long GRBs. The afterglows of short bursts may therefore be quite different. If there is no cocoon then jets from short bursts may have very little baryon loading. The prompt emission might also be produced by some other mechanism. Additionally, the environment surrounding short bursts may be very different from a $k = 2$ wind, so even if a coasting phase is detected, this phase might be characterized by a rise instead of a plateau.

Some short bursts are followed by a long tail of extended emission (Norris & Bonnell 2006; Perley et al. 2009) that might be interpreted as an afterglow. (However, extended emission can exhibit rapid variability, which is not accounted for in this model.) If the environment of the burst is uniform ($k = 0$), then instead of a plateau one would expect a rise $\propto t^2$, followed by a decay consistent with Blandford–McKee. The peak of the light curve would occur at the deceleration time,

$$t_{\text{peak}} \sim \left( \frac{E_{\text{iso}}}{\rho_{\text{ISM}} c^5} \right)^{1/3}. \quad (20)$$

The examples of GRB 050724 and others (Gompertz et al. 2014) have extended emission with peak times of $\sim 100$ seconds. Under this interpretation, assuming $E_{\text{iso}} = 10^{51}$ erg and $\rho_{\text{ISM}} = 10^{-24}$ g cm$^{-3}$, one would infer a jet Lorentz factor

$$\Gamma \sim \left( \frac{E_{\text{iso}}}{\rho_{\text{ISM}} c^5 t_{\text{peak}}} \right)^{1/8} \approx 100. \quad (21)$$

This large inferred Lorentz factor would suggest that either the core initially has a much larger Lorentz factor, $\Gamma_{\text{core}} \sim 10^3$, before colliding with an outer shell and decelerating to $\Gamma \sim 100$, or that short bursts simply produce jets that are not top-heavy.

5. SUMMARY

Collapsars naturally produce top-heavy outflows; a highly relativistic jet core is associated with the clean outflow escaping via the passageway tunneled out by the engine. A less relativistic component is associated with the baryon-loaded outer shell of the jet which was originally in front of the jet head at breakout.

A collision between these two flows can produce a flare (possibly prompt emission) at early observer times, followed by a steep decay in the afterglow until $t_{\text{obs}} \sim 100$ s, as seen in Swift light curves. The jet core is relativistic enough to produce the prompt emission with $\Gamma_{\text{core}} \sim 100$, but the late afterglow is produced by a much less relativistic jet, formed from the amalgamation of the shell and core. Because of the lower Lorentz factor ($\Gamma \sim 30$) of the less relativistic afterglow, the deceleration time of the jet occurs at the relatively late observer time $t_{\text{obs}} \sim 10^{4.5-5}$ s, and during the time in-between internal shocks and deceleration, the afterglow can exhibit a long plateau, as seen in Figure 6.

This model represents both a natural mechanism for the steep decay seen at early times, and an alternative to the late-time energy injection model to explain plateaus in GRB afterglow light curves. This model is purely hydrodynamic (magnetic fields are neglected), suggesting that hydro models may be accurate for most of the jet’s propagation through the star, consistent with recent analysis (Bromberg et al. 2014). Beyond the usual collapsar scenario, no new ingredients are imposed in this model; top-heavy jets naturally arise when the jet collimation is facilitated by a stellar interior.

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