Effect of Magnetic Field on Dilepton Production Rate in Relativistic Heavy Ion Collisions

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Abstract

It is believed that a transient strong magnetic field is generated in heavy-ion collision. The strength of this field perpendicular to the reaction plane and is estimated to be around eB=0.03GeV² at RHIC and eB=0.3GeV² at LHC. We study the effect of this magnetic field on dilepton yield using a modified quasi particle model. The results show a clear enhancement in dilepton yield and our result is in good agreement with the recently reported results.

Keywords: Quark-Gluon Plasma; QCD; Dilepton; Heavy-ion collision.

1. Introduction

The contradiction between the limiting temperature concept of hadronic matter from Hegedron model and monotonically increase of energy density with collision energy concept from Fermi-Landau-Pomeranchuk model, indicates existence of a deconfined quark phase. Relativistic heavy-ion collision experiments have confirmed the presence of strongly coupled matter- Quark-Gluon Plasma (QGP) [1-3]. Due to considerable interaction strength this system of liberated quarks and gluons reaches its thermalized state early. This thermalized quark matter expands and gradually cools down as the system evolves with time and beyond a critical temperature it converts into hadronic matter. The hadron gas further expands to reduce energy density and finally reaches the freeze-out.

The contemporary physics provides a theoretical platform to understand the many-body physics of Quantum Chromodynamics (QCD). QCD matter at low temperature and density is composed of hadrons, while at high temperature and high density; it is

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believed that the deconfinement of quarks and gluons takes place. The wealth of
information provided by the Relativistic Heavy Ion Collider (RHIC) at Brookhaven
National Laboratory (BNL) and by the Large Hadron Collider (LHC) at CERN has
confirmed the formation of such a QCD matter-hot quark-gluon plasma (QGP). The
off-central heavy-ion collision produce large electromagnetic fields [4,5]. Strong
magnetic field has also been estimated in noncentral heavy-ion collisions [6-9]. When
two heavy ion nuclei approach towards each other generate two electric currents in
opposite directions and eventually produce a large time dependent magnetic field
perpendicular to the collision plane. Using Biot-Savart formulae, a naive estimation of
the magnetic field can be made. In RHIC, Au + Au collisions at \( s = \sqrt{200} \) GeV has
reported the magnetic field produced is in the order of \( 10^{19} \) Gauss and in LHC Pb + Pb
collisions at \( s = \sqrt{2.76} \) TeV the magnetic field is of the order of \( 10^{20} \) Gauss [10-12].
Thus the experimental results reported by PHENIX at RHIC (\( E \leq 200 \)GeV) established
the fact that a transient strong magnetic field is created in heavy-ion collision. This
magnetic field is much larger than the mass squared of light quarks and thus are
expected to affect the dynamics of the quark-gluon plasma significantly. This field is
found to be much above Schwinger critical value. In this regime the classical
electrodynamics breaks down. Due to high temperature and density, the direct access
of QGP properties is not very feasible. Only information is available from the final
state particle spectra. Therefore, it is imperative to study the magnetic field induced
dilepton production in heavy-ion collision. The magnitude of the magnetic field
produced is found to be linearly dependent on the collision energy [13-15] and this is
evident from Lorentz gamma factor appearing in Biot-Savart formulae:

\[
eB = \frac{\gamma \alpha Z}{R^2_A}
\]

A relativistic electron carries with it a virtual photon spectrum of photons per unit
frequency interval. When radiation occurs, for whatever reason, the observed
frequency spectrum will closely follow this virtual spectrum. In cases where the
driving force for the radiation extends over many formation lengths, the spectrum of
radiated photons per unit path length for intense processes which describe the radiation
emitted over one formation length, divided by the formation length [16]. This is
referred to as Weizsacker-William’s approximation and is useful to compute the
dilepton yield with logarithmic accuracy. Initially just after the collision of heavy
ions, the initial distribution of soft (\( E < T \)) and hard quarks (\( E > T \) and \( Q_s > T \)) would
be a decisive factor for the subsequent stage of emission of lepton pair. The dilepton
yield is calculated for \( T < E < Q_s \). The reason for considering this zone is that the soft
quark spectrum falls off in an exponential manner whereas the hard quark spectrum is
logarithmic. The numbers of soft quarks are proportional to the \( T^3 \) and volume of the
plasma. The number of hard quarks is proportional to square of the saturation
momenta. At early times, the volume of the plasma is also proportional to the cross-
sectional area of heavy ion overlap region. The magnetic field in quark-gluon plasma
appears to be extremely strong and slowly varying function of time for most of the
plasma lifetime. At RHIC it decreases from eB(=2.5GeV$^2$) right after the collision to eB(=0.25GeV$^2$). This has a profound impact on all the processes occurring in QGP. The exotic state of matter is created along with a huge magnetic field. Thus, it offers a great opportunity to observe the interaction of this magnetic field with the quark-gluon plasma. Here we try to calculate the dilepton production rate with reference to the response of the QGP to the electromagnetic field.

In this paper we compute the dilepton production rate from the quark-gluon plasma in the presence of magnetic field. We envisage the situation from a different perspective. Firstly, we consider the exotic state of matter as a system of quasi particles. The quarks acquire a dynamic mass in this system due to interaction. This quark mass is considered to be temperature dependent. It has been well established that there is strong magnetic field generated at the early time of the heavy ion collisions. This magnetic field would affect the dynamics of QGP. Therefore, it is pertinent to study the effect of this magnetic field on the dilepton yield.

The structure of our paper is as follows. In section 2 we calculate production rate of dileptons at finite temperature $T$ and quark chemical potential, $\mu$ in the inherent magnetic field and brief model description. In Section 3 we present our results and compare them with some other theoretical results.

2. Calculation of Dilepton Emission Rate and Model Description

In heavy-ion collision, dileptons are produced from quarks (or antiquarks) through the mediation of a virtual photon. Here we consider a process where both the quark and the lepton move in the magnetic field created during the heavy-ion collision. Although there may be another possibility in which either the quark or the lepton moves in the magnetic field [17]. But it is believed that the earlier one (both quark and lepton move) is most sensitive to the prevailing magnetic field in heavy-ion collision [18].

At RHIC and LHC, the centre-of-mass energy per nucleon is larger than the ratio of nucleon mass to the product of nuclear radius and electrical conductivity. This condition is based on a reasonable approximation that the time dependence of the magnetic field is adiabatic [19]. The relativistic electron has the electromagnetic field which is very similar to the fields of a plane wave. Therefore, we can consider the relativistic electron as if a cloud of virtual photons is carried by it and has the ability to radiate. Weiszacker and Williams estimated the energy response and the number of photons corresponding to a particular frequency. Essentially the observed frequency spectrum in a radiation process keeps on following the spectrum of virtual photons carried by the relativistic electron. There are several approaches to understand the interaction of charged particles. It is quite easy to describe such interaction when the speed of the particles is nearly the speed of light. In relativistic domain, one observes the contraction of electric E and magnetic B fields of such a particle into the plane that is perpendicular to the direction of motion. The magnitude of E and B fields are nearly the same and are perpendicular to one another. For an observer at rest, at certain
distance away from the passing particle, the effects of these fields appear to be indistinguishable from those of a passing EM wave. In such circumstances, approximation of the particles EM fields as EM plane waves helps us to analyze the interaction of two ultra-relativistic (UR) charged particles. Thus, the non-central collision of two UR particles can be equivalently treated as the interaction between an UR particle and a passing EM wave [20]. Weiszacker method is useful to write down the flux of the photons emitted by a fast quark. With the above approximations, the dilepton production rate can be written as:

$$\frac{dN_q}{dtd\Omega dE} = \int n(\omega) \frac{dN_{\gamma}}{dtd\Omega dE} d\omega$$

where $n(\omega)$ is the flux of equivalent real photon replacing virtual photon. The expression for $n(\omega)$ is given by,

$$n(\omega) = \frac{2Z_q^2 \alpha}{\pi \omega} \ln \frac{E}{\omega} \left[ 1 + \frac{\omega}{\omega} \right]$$

It has been realised that in the relativistic heavy-ion collisions, there is a significant contribution of finite baryon chemical potential in central collision. This finite baryon chemical potential $\mu$ is reported to be at energies around $\sqrt{s} \leq 200$ AGeV. It is further reported by the microscopic models [21,22] that the colliding heavy-ions may not be fully transparent. The significance of chemical potential produced at RHIC energy has been reported by Hammon et al. [23]. It is believed that there exists non-zero chemical potential in the early stage of the plasma. This information prompted Dumitru et al. to express dilepton emission rate as a function of temperature and quark chemical potential $\mu$ of the QGP [24]. We define quark mass which depends on temperature and chemical potential and it is expressed as,

$$m_q^2(T, \mu) = \frac{N_f^2}{16N_c} \left( T^2 + \frac{\mu^2}{\pi^2} \right) \frac{g^2}{\alpha_s}$$

where $g^2 = 4\pi\alpha_s$ is the QCD coupling factor and the value of $\alpha_s$ is given as,

$$\alpha_s = \frac{4}{(33 - 2N_f) \ln \left( 1 + \frac{k^2}{\Lambda^2} \right)}$$

Here $\Lambda$ is QCD parameter, $N_f$ is the number of quark flavour and $k$ is the momentum value. When the plasma is exposed to magnetic field, the quark mass is suitably modified to $m_{\text{eff}}^B$ - Magnetized Effective Quark Mass (MEQM). The expression for the magnetized effective quark mass is [25]:

$$m_{\text{eff}}^B = m_{\text{eff}}^2 + eB(2n + s + 1)$$

Where $m_{\text{eff}}$ is given by Ref. [26,27],

$$m_{\text{eff}}^2 = m_c^2 + \sqrt{2}m_c m_q + m_q^2$$
The parameter $m_c$ and $m_q$ are the current and thermal mass of the quark. The estimated magnetic field can be expressed as:

$$eB = \frac{\alpha z R \sigma}{t^2} \exp \left( -\frac{R^2 \sigma}{4t} \right)$$

In such a scenario, the single particle energy eigen value is given by [28,29],

$$E^B = \left[ m_{\text{eff}}^B + k^2 \right]^{1/2}$$

Realizing the dependence of dilepton yield on rapidity, collision energy, saturation momentum, valence quark distribution function and some phenomenological parameter, one can simplify the expression for dilepton production rate as [30]:

$$\frac{dN_{\gamma \rightarrow \ell^{+}\ell^{-}}}{dt d\Omega dE} = \frac{NSQ^2 \alpha^2 m_i^2}{3\pi^3} \sum_{i=0}^{\infty} Z_q \int d\beta \int \frac{d\omega}{\omega} \left[ \frac{E}{\omega} \ln \frac{E}{\omega[1 + (\chi E / \omega)^{1/3}]} \right] \frac{2}{x - \chi x^{1/3}} \text{Ai}(x)$$

3. Results

Magnetic field generated in heavy-ion collisions has a profound impact on dilepton production. Indeed, magnetic field strength by far exceeds the critical Schwingers value during the entire QGP lifetime. The effective quark mass in the presence of magnetic field (B=0.03-0.3 GeV$^2$) shows very similar result for dilepton yield with the recent result of Tuchin et al. Our model result also shows an enhanced dilepton yield in low invariant mass region as comparison to high mass region. Fig. 1 depicts the dilepton yield with the effective quark mass at different energy with the inclusion of magnetic field and we try to show a comparative dilepton yield. In this it is pertinent that there is an enhanced value. We attribute this enhanced value to the magnetized effective quark mass.

![Fig. 1. Comparative dilepton yield with respect to energy at eB=0.03GeV$^2$.](image)
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