Generation of models from existing models composition: An application to agrarian sciences

André Luiz Pinto dos Santos¹, Guilherme Rocha Moreira¹, Frank Gomes-Silva⁰¹*, Cícero Carlos Ramos de Brito², Maria Lindomárcia Leonardo da Costa³, Luiz Gustavo Ribeiro Pereira⁴, Rogério Martins Maurício⁵, José Augusto Gomes Azevêdo⁶, José Marques Pereira⁷, Alexandre Lima Ferreira⁵, Moacyr Cunha Filho¹

¹ Department of statistics and informatics, Federal Rural University of Pernambuco, Recife, Pernambuco, Brazil, ² Federal Institute of Pernambuco, Recife, Pernambuco, Brazil, ³ Animal Science Department, Federal University of Paraíba, Areia, Paraíba, Brazil, ⁴ Embrapa Dairy Cattle, Juiz de Fora, Minas Gerais, Brazil, ⁵ Bioengineering Department, Federal University of São João del-Rei, São João del-Rei, Brazil, ⁶ Universidade Estadual de Santa Cruz, Ilhéus, BA, Brazil, ⁷ CEPLAC-ESSUL, Itabela, Bahia, Brazil

* franksinatrags@gmail.com

Abstract

Mathematical models that describe gas production are widely used to estimate the rumen degradation digestibility and kinetics. The present study presents a method to generate models by combining existing models and to propose the von Bertalanffy-Gompertz two-compartment model based on this method. The proposed model was compared with the logistic two-compartment one to indicate which best describes the kinetic curve of gas production through the semi-automated in vitro technique from different pinto peanut cultivars. The data came from an experiment grown and harvested at the Far South Animal Sciences station (Essul) in Itabela, BA, Brazil and gas production was read at 2, 4, 6, 8, 10, 12, 14, 17, 20, 24, 28, 32, 48, 72, and 96 h after the start of the in vitro fermentation process. The parameters were estimated by the least squares method using the iterative Gauss-Newton process in the software R version 3.4.1. The best model to describe gas accumulation was based on the adjusted coefficient of determination, residual mean squares, mean absolute deviation, Akaike information criterion, and Bayesian information criterion. The von Bertalanffy-Gompertz two-compartment model had the best fit to describe the cumulative gas production over time according to the methodology and conditions of the present study.

Introduction

Brazil has capacity and demand for the use of forage grasses as the main source of food in animal nutrition. However, the production capacity, nutritional value, and rumen degradation of the grass must be known to guide decisions to meet the nutritional needs of ruminants [1]. Diet formulation systems require knowing the nutritional value of foods, among which forage grasses. The kinetic parameters of degradation are important as they describe the digestion and characterize the intrinsic properties of foods that limit the availability to ruminants [2].
As reported by [3], several non-linear models are used to estimate the rumen fermentation kinetics of foods. A major advantage of those models is the possibility of biological interpretation of parameters [4]. However, when growth has a characteristic behavior that enables identifying steps, which allow dividing the curve into several stages, adopting multi-compartment models becomes necessary as they take exclusive parameters into account for each compartment [5].

A logistic two-compartment (LB) model was developed by [6] for kinetic studies of *in vitro* gas production based on the assumption that production rate is impacted by microbial mass and substrate level. Several researchers have used that model to study the kinetics of cumulative gas production [7,8]. However, the logistic model may not be adequate for some cases due to its fixed inflection point halfway through cumulative gas production [9]. [9,10] concluded that new models are still needed that can yield more biologically significant results with good mathematical fit of broad ranges of curve shapes with variable inflection points. In addition, creating new models for overall and specific situations is highly justifiable in face of the dynamics with which non-linear models have been applied in biological researches [11,12,13].

Thus, this study presents a method to generate growth and degrowth models by combining existing models and, specifically, to propose a new two-compartment model from the combination of the von Bertalanffy and Gompertz models. The logistic two-compartment model and the proposed one were compared to identify which has the best fit to cumulative gas production curves of ten genotypes of pinto peanut (*Arachis pintoi*) used in ruminant feed.

### Material and methods

#### Data used

The genotypes were grown and harvested at the animal science station of CEPLAC in Itabela, BA, Brazil, a region located at 100 m altitude, 16˚36’ S, and 39˚30’ W featuring mean annual temperature of 23.3 °C and 1,350 mm of rainfall with no defined dry season. The genotypes were harvested in the rainier season. A randomized block experimental design with ten pinto peanut genotypes and three replicates was employed. The treatments comprised ten *Arachis pintoi* cultivars, namely: 13251 (G1), 15121 (G2), 15598 (G3), 30333 (G4), 31135 (G5), 31496 (G6), 31534 (G7), 31828 (G8), Itabela (G9), and Rio (G10). The genotypes were planted in beds with total area of 4 m² and useful area of 1 m². To obtain the dry matter (DM) and green matter (GM) production per hectare in both periods, the plants were cut 5 cm from the ground and, after the green forage was weighed, it was taken to the Animal Nutrition laboratory of the State University of Santa Cruz–UESC, where it was dried in a forced air circulation oven at mean temperature of 55 °C for 48 h and then ground in a Willey knife mill equipped with 1 mm sieve. The DM content at 105 °C was determined by drying until constant weight, crude protein (CP) and acid detergent insoluble protein (ADIP) were defined using the Kjeldahl method according to the AOAC [14], and neutral detergent fiber (NDF) and acid detergent fiber (ADF) were determined according to [15]. Gas production was read at 2, 4, 6, 8, 10, 12, 14, 17, 20, 24, 28, 32, 48, 72, and 96 h after the start of the *in vitro* fermentation process at the Federal University of Minas Gerais (UFMG) according to the equation proposed by [16].

#### Method to generate growth and degrowth models by combining existing models

This section is one of the main objectives of our work. It consists in generalizing combination methods applied to agrarian sciences. These methods have been disseminated over several
years in this area of science and, in the present work, in addition to gathering them, we provide other possible methods that, to the extent of our knowledge, have not been explored yet.

Let \( W_1(t_1, \ldots, t_k), \ldots, W_n(t_1, \ldots, t_k) \) be existing models in the literature and consider \( f : \mathbb{R}^n_+ \to \mathbb{R} \) a function. Then

\[
W(t_1, \ldots, t_k) = f(W_1(t_1, \ldots, t_k), \ldots, W_n(t_1, \ldots, t_k))
\]

is a combination of such models via said function. Depending on the function, we can obtain several model-building methods, such as the ones below:

1. **Method to generate growth and degrowth models via combinations in the weighted sums of power of models or linear combinations of power of existing models.**

   Let \( W_1(t_1, \ldots, t_k), \ldots, W_n(t_1, \ldots, t_k) \) be existing models in the literature. Consider

   \[
   f(x_1, \ldots, x_n) = \sum_{j=1}^{n} \alpha_j \cdot x_j^b, \quad x_1 = W_1(t_1, \ldots, t_k), \ldots, x_n = W_n(t_1, \ldots, t_k),
   \]

   then:

   \[
   W(t_1, \ldots, t_k) = f(W_1(t_1, \ldots, t_k), \ldots, W_n(t_1, \ldots, t_k)) = \sum_{j=1}^{n} \alpha_j \cdot W_j^b(t_1, \ldots, t_k).
   \]

   Therefore, for such function \( f \), the building method is given by:

   \[
   W(t_1, \ldots, t_k) = \sum_{j=1}^{n} \alpha_j \cdot W_j^b(t_1, \ldots, t_k). \tag{2}
   \]

2. **Method to generate growth and degrowth models via combinations in the product of powers of existing models.**

   In this case, use the function

   \[
   f(x_1, \ldots, x_n) = \alpha \cdot \prod_{j=1}^{n} x_j^b
   \]

   to obtain as building method

   \[
   W(t_1, \ldots, t_k) = \alpha \cdot \prod_{j=1}^{n} W_j^b(t_1, \ldots, t_k). \tag{3}
   \]

3. **Method to generate growth and degrowth models via combinations in the sum of products of existing models.**

   In this case, simply use the function

   \[
   f(x_1, \ldots, x_{mn}) = \sum_{j=1}^{n} \left( \alpha_j \prod_{i=1}^{m} x_i^{b_j} \right)
   \]

   to obtain as building method

   \[
   W(t_1, \ldots, t_k) = \sum_{j=1}^{n} \left( \alpha_j \prod_{i=1}^{m} W_i^{b_j} (t_1, \ldots, t_k) \right). \tag{4}
   \]

4. **Method to generate growth and degrowth models via combinations of the product of sums of existing models.**

   In this case, we should consider the function

   \[
   f(x_1, \ldots, x_{mn}) = \prod_{j=1}^{n} \left( \sum_{i=1}^{m} \alpha_i \cdot x_i^{b_j} \right)^{\frac{1}{\sum_{i=1}^{m} \alpha_i}}
   \]
to obtain as building method
\[ W(t_1, \ldots, t_k) = \prod_{j=1}^{n} \left( \sum_{i=1}^{m} x_i \cdot W_i^b(t_1, \ldots, t_k) \right)^{j_x}. \] (5)

5. **Method to generate growth and degrowth models via combinations in the sum of powers added to the product of powers of existing models.**

In this case, simply use the function
\[ f(x_1, \ldots, x_{m+n}) = \sum_{j=1}^{n} x_j^b \cdot \left( \sum_{i=1}^{m} x_i^b \right)^{j_x} \]
to obtain as building method
\[ W(t_1, \ldots, t_k) = \sum_{j=1}^{n} x_j W_j^b(t_1, \ldots, t_k) + \sum_{i=1}^{m+n} W_i^b(t_1, \ldots, t_k). \] (6)

6. **Method to generate growth and degrowth models via combinations in the sum of powers of sums of existing models.**

The function stated as
\[ f(x_1, \ldots, x_{m+n}) = \sum_{j=1}^{n} x_j^b \cdot \left( \sum_{i=1}^{m} x_i^b \right)^{j_x} \]
should be considered to obtain as building method
\[ W(t_1, \ldots, t_k) = \sum_{j=1}^{n} x_j \cdot \left( \sum_{i=1}^{m} W_i^b(t_1, \ldots, t_k) \right)^{j_x}. \] (7)

7. **Method to generate growth and degrowth models via combinations in adding parameters to existing models.**

Another building method occurs when parameters are added to an existing model. If \( W_1 = W_1(t_1, \ldots, t_k/\beta_1, \ldots, \beta_m), \ldots, W_n = W_n(t_1, \ldots, t_k/\beta_1, \ldots, \beta_m) \) are existing models, then for each function \( f \) and extra parameters \( \beta_{m+1}, \ldots, \beta_{m+r} \), we can determine the building method:
\[ W(t_1, \ldots, t_k/\beta_1, \ldots, \beta_{m+r}) = f(W_1, \ldots, W_n/\beta_{m+1}, \ldots, \beta_{m+r}). \] (8)

It can be seen that our method has a very broad character since Eq (1) may contemplate not only the time variable, but also other important variables for the comprehension of growth dynamics. Next, we present a “byproduct” of our method and illustrate it based on a numeric application.

**Proposed model and theoretical application**

von Bertalanffy and Gompertz are basic models widely used to fit growth curves. The Gompertz model has been developed to describe microbial growth and was first used by [6] to study the kinetics of in vitro gas production [10]. These models were used in studies such as those by [17,18] for cumulative gas production kinetics. More recently, [13] presented the von Bertalanffy and Gompertz models, among others, (see Table 1, p. 2664) as sub-cases of what they called the method to generate growth models obtained from differential equations. Thus,
the development of the mathematical model proposed resulted from the combination of the two models:

- von Bertalanffy:

\[
W_1(t) = \alpha_1 (1 - \beta_1 e^{k_1 t})^\gamma + \varepsilon
\]

(9)

- Gompertz:

\[
W_2(t) = \alpha_2 e^{-\beta_2 e^{-k_2 t}} + \varepsilon.
\]

(10)

Indeed, let \( W(t) \) be an estimate of growth of the accumulated gas volume, hence, by building method (i) given by Eq (2), we can describe:

\[
W(t) = W_1(t) + W_2(t) = \alpha_1 (1 - \beta_1 e^{k_1 t})^\gamma + \alpha_2 e^{-\beta_2 e^{-k_2 t}} + \varepsilon.
\]

(11)

Thus, Eq (11) consists of our proposed model, called Two-Compartment von Bertalanffy-Gompertz model, or VGB, as it is a combination of Eqs (9) and (10). Analogously, by observing the building methods provided in Section 2.2, we can generate one- or two-compartment models found in the literature, some of which fitted to in vitro gas production and others with potential application in this area, as described in Table 1.

In these models, \( W(t) \) is the accumulated volume (mL) at time \( t \); \( \alpha \) is the gas volume corresponding to complete substrate digestion (mL); \( \alpha_1 \) is the gas volume produced from the rapid-digestion fraction of non-fiber carbohydrates (NFC); \( \alpha_2 \) is the gas volume produced from the slow-digestion fraction of fiber carbohydrates (FC); \( \lambda \), \( \beta_1 \), and \( \beta_2 \) are shape parameters with no biological interpretation; \( k_1 \) is the specific rate of gas production; \( k \) is the degradation rate of the rapid-digestion fraction (NFC); \( k_2 \) is the degradation rate of the slow-digestion fraction (FC); \( t \) is the fermentation time; \( \varepsilon \) is exponential; and \( \varepsilon \) is the random error associated with each observation with normal distribution, zero means, and constant variance. Thus, the cumulative gas production kinetics was fitted using models VGB and LB.

Table 1. One- and two-compartment models from the methods.

| Unicompartmental models | Building method | Models generated |
|-------------------------|-----------------|-----------------|
| Brito-Silva [11]        | (ii)            | \( W(t) = \alpha_2 (1 + \beta_1 e^{-k_1 t}) (1 + \beta_1 e^{-k_2 t}) \) + \( \varepsilon \) |
| Exponential [17]        | (vii)           | \( W(t) = \alpha_1 (1 - e^{-k_1 t}) + \alpha_2 e^{-\beta_2 e^{-k_2 t}} + \varepsilon \) |
| Logarithmic [17]        | (vii)           | \( W(t) = \alpha_1 (1 + \beta_1 e^{-k_1 t}) + \lambda + \beta_2 e^{-k_2 t} + \varepsilon \) |
| Gompertz [17]           | (vii)           | \( W(t) = \alpha_2 e^{-\beta_2 e^{-k_2 t}} + \varepsilon \) |

| Two-compartment models  | Building method | Models generated |
|-------------------------|-----------------|-----------------|
| Exponential-Logistic [19]| (i)             | \( W(t) = \alpha_1 (1 - e^{-k_1 t}) + \alpha_2 e^{-\beta_2 e^{-k_2 t}} + \varepsilon \) |
| Michaelis-Menten [17]   | (i)             | \( W(t) = \alpha_2 (1 + \beta_1 e^{-k_1 t}) + \lambda + \beta_2 e^{-k_2 t} + \varepsilon \) |
| Gompertz Two-compartment [17] | (i) | \( W(t) = \alpha_2 e^{-\beta_2 e^{-k_2 t}} + \alpha_2 e^{-\beta_2 e^{-k_2 t}} + \varepsilon \) |
| Exponential Two-compartment [20] | (i) | \( W(t) = \alpha_1 (1 - e^{-k_1 t}) + \lambda + \beta_2 e^{-k_2 t} + \varepsilon \) |
| Logistic Two-compartment [6] | (i) | \( W(t) = \alpha_2 (1 + \beta_1 e^{-k_1 t}) + \lambda + \beta_2 e^{-k_2 t} + \varepsilon \) |

https://doi.org/10.1371/journal.pone.0214778.t001
Estimating parameters of non-Linear models, assessors of goodness-of-fit, and test of model identity and parameter equality

Next, the kinetics parameters of non-linear models VGB and LB were estimated via the least-squares method using the iterative Gauss Newton process through the function Nonlinear Least Squares. The statistical analyses were carried out using the software R version 3.4.1 [21].

To assess which model had the best fit, we used the following assessors: adjusted coefficient of determination ($R_{adj}^2$), residual mean squares (RMS), mean absolute deviation (MAD), Akaike information criterion (AIC), and Bayesian information criterion (BIC) according to Table 2.

The terms that appear in Table 2 are described as follows: $SS_{res}$ is the sum of the squares of the residues defined by $SS_{res} = \sum_{i=1}^{n} (y_i - \hat{y}_i)^2$, where $y_i$ is the volume observed and $\hat{y}_i$ is the volume estimated (prediction) of $y_i$; $n$ is the number of observations, and $p$ is the number of free parameters of the model. It is considered that lower values for RMS, AIC, BIC, and MAD and the highest $R_{adj}^2$ value, the better the fit.

Results and discussion

The cumulative gas production curves obtained from the observed and fitted data of genotypes of pinto peanut for both models had sigmoid shape over time and can be split into three stages, namely: initial stage of low gas production; exponential stage of rapid gas production; and asymptotically null stage or low gas production (Fig 1).

Models LB and VGB fitted to all stages of the fermentation process of genotypes G1, G2, G4, G5, G7, G8, G9, and G10. For genotypes G3 and G6, the models showed good fits both in the initial portion of the curve and in the exponential stage, but there is evidence they did not have good fits to the asymptotic phase, in which gas production was over- or underestimated, respectively, by the LB and VGB models. However, model behavior also largely depends on the morphological [22] and chemical [23] characteristics employed. The same model may have low or high performance when using genotypes of the same species or when using different substrates [18].

Considering all genotypes, estimates $\hat{x}_1$ and $\hat{x}_2$ for model LB were higher and lower, respectively, than estimates $\hat{x}_1$ and $\hat{x}_2$ for model VGB. The final gas volume $W(t)$ is produced by the rapid- and slow-digestion fractions, i.e., the sum of NCF and FC. Genotype G4 had the lowest total gas volume $W(t)$ for models VGB and LB, whereas genotype G7 and G9 had the highest values for both models.

[26] found high accumulated gas production for corn and sunflower silages and their combinations (0, 25; 50 and 100%). Forage peanut contain some soluble carbohydrates [28] and according to [29], the volume of gases produced depends on substrate composition, i.e., the higher the starch and fiber contents, the lower and higher their gas productions, respectively.

Table 2. Mathematical description of the selection criteria.

| Equations                                                                                   |
|---------------------------------------------------------------------------------------------|
| $R_{adj}^2 = R^2(1 - (1 - R^2)n - 1)$                                                       |
| $MAD = \frac{\sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{n - p}$                                  |
| $RMS = \frac{\sum_{i=1}^{n} |y_i - \hat{y}_i|}{n}$                                         |
| $AIC = n + n\log(2\pi) + n\log(SS_{res}/n) + 2(p + 1)$                                    |
| $BIC = n + n\log(2\pi) + n\log(SS_{res}/n) + (\log n)(p + 1)$                             |

https://doi.org/10.1371/journal.pone.0214778.t002
Probably the smallest gas volume production by genotypes in this research is explained for the lower soluble carbohydrate content when compared to corn and sunflower silages [30].

According to Table 3, the estimated rates of rapid and slow degradation of the NFC and FC were 0.20 and 0.04 for the VGB model and 0.07 and 0.02 for the LB model, noting the
dissimilarity among the genotypes for the two models evaluated with higher values for VGB.

The estimated degradation rate values $k_1$ and $k_2$ of the VGB model were similar to those found by [31] for different forage grasses. Those authors reported values of 0.095 (0.04), 0.108 (0.04), 0.131 (0.04), 0.203 (0.04), 0.216 (0.04), and 0.222 (0.04) for silages of corn, alfalfa hay, sorghum, sugar cane, Coastcross hay, and Tifton-85, grass, respectively. The estimated degradation rates $k_1$ and $k_2$ by model LB were similar to those found by [24,25] for pinto peanut genotypes.

Another relevant piece of information is that $k_1 > k_2$ for the models fitted considering all genotypes (Table 3). That matches the important aspect of the theory according to which

![Image of Normality plots of the statistical model through the residues for all genotypes.](https://doi.org/10.1371/journal.pone.0214778.g003)

Table 3. Estimated values of parameters $\alpha_1, \alpha_2, k_1, k_2$, and $\lambda$ for the VGB and LB models fitted to data on pinto peanut genotypes.

| Genotypes | Estimates (VGB) | Estimates (LB) |
|-----------|-----------------|----------------|
|           | $\hat{\alpha}_1$ | $\hat{\alpha}_2$ | $\hat{k}_1$ | $\hat{k}_2$ | $\hat{\alpha}_1$ | $\hat{\alpha}_2$ | $\hat{k}_1$ | $\hat{k}_2$ | $\hat{\lambda}$ |
| G1        | 75.05           | 63.45           | 0.20        | 0.04        | 89.13           | 45.73           | 0.07        | 0.02        | 4.52          |
| G2        | 75.75           | 57.91           | 0.20        | 0.04        | 89.30           | 41.42           | 0.07        | 0.02        | 4.40          |
| G3        | 85.09           | 61.49           | 0.20        | 0.03        | 93.44           | 48.30           | 0.07        | 0.02        | 5.46          |
| G4        | 63.73           | 54.21           | 0.20        | 0.04        | 75.02           | 39.75           | 0.07        | 0.02        | 4.84          |
| G5        | 77.72           | 61.05           | 0.20        | 0.04        | 89.70           | 45.34           | 0.07        | 0.02        | 4.78          |
| G6        | 71.53           | 57.56           | 0.20        | 0.04        | 84.64           | 41.21           | 0.07        | 0.02        | 4.77          |
| G7        | 87.25           | 68.42           | 0.20        | 0.04        | 101.63          | 50.15           | 0.07        | 0.02        | 4.91          |
| G8        | 80.70           | 68.56           | 0.20        | 0.04        | 94.78           | 50.84           | 0.07        | 0.02        | 5.01          |
| G9        | 91.55           | 69.37           | 0.20        | 0.04        | 106.00          | 51.34           | 0.07        | 0.02        | 4.88          |
| G10       | 83.01           | 68.37           | 0.20        | 0.04        | 101.00          | 47.62           | 0.06        | 0.02        | 4.67          |

https://doi.org/10.1371/journal.pone.0214778.t003
parameter $k_1$ is greater than parameter $k_2$, i.e., NFC are more quickly degraded than FC [6,32]. [33] used this recommendation in their study.

The highest rates of gas production observed in this study showed the importance of the forages legume crop like forage peanut (Arachis pintoi) for agricultural production systems. According to [28] these plants increase the input of nitrogen through biological nitrogen fixation, help control pests and diseases and control soil erosion by their persistence in the pasture and present high nutritional value for animals.

In vitro gas production techniques have attracted the attention of researchers from different areas of the world, and from different disciplines, that study direct or indirect impacts of animal production on the environment [34]. In vitro gas accumulation measurements provide valuable information about the kinetics of feed digestion in rumen fluid. Mathematical models are necessary tools to describe and interpret in vitro gas production kinetics [10]. However, have questions about which is the most appropriate model. The evaluation of the quality of adjustments of these models can be done several ways [35, 13].

The goodness-of-fit assessors are presented in Table 4. Choosing the best models has not been an easy task since each of the different goodness-of-fit assessors proposed in the literature recommends a certain characteristic such as model simplicity [36]. However, the higher the number of assessors considered, the more adequate the indication of the best model(s) [37]. A comparison of the two models showed the smallest differences were found for $R^2_{adj}$, whose values were very close for both models, with no evidence of which has the best fit. Nevertheless, for all genotypes, when criteria RMS, MAD, AIC, and BIC were analyzed, we observed that the VGB model had the lowest values (Table 4). The best fitted model is the one that has the lowest values for RMS, AIC, BIC, and MAD and the highest $R^2_{adj}$ value. Therefore, the information favors indicating the best fits to the proposed model.

Few papers are found in the literature that reference studies on mathematical models for in vitro gas production using pinto peanut genotypes. [38], when comparing several models to assess pinto peanut genotypes during the rainy and less rainy seasons in Itabela, BA, Brazil, found the best fit through LB, followed by the von Bertalanffy, Gompertz, Brody, and Logistic models. Meanwhile, [17], when assessing the Brody, von Bertalanffy, Gompertz, France, logistic, modified logistic, and LB models to describe cumulative gas production in sunflower and corn silages, concluded the LB was the best model. According to [6,39], multi-compartment models had better goodness-of-fit than those based on first-order kinetics.

| Criteria          | G1       | G2       | G3       | G4       | G5       | G6       | G7       | G8       | G9       | G10      |
|-------------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| $R^2_{adj, LB}$   | 0.9991   | 0.9993   | 0.9992   | 0.9990   | 0.9992   | 0.9991   | 0.9993   | 0.9991   | 0.9993   | 0.9992   |
| $R^2_{adj, VGB}$  | 0.9994   | 0.9995   | 0.9995   | 0.9994   | 0.9995   | 0.9994   | 0.9994   | 0.9995   | 0.9995   | 0.9993   |
| RMS$_{LB}$        | 2.70     | 2.01     | 2.73     | 2.12     | 2.51     | 2.27     | 2.82     | 3.18     | 3.02     | 3.02     |
| RMS$_{VGB}$       | 1.63     | 1.42     | 1.91     | 1.40     | 1.50     | 1.87     | 2.22     | 2.02     | 2.27     | 2.53     |
| MAD$_{LB}$        | 1.03     | 0.88     | 1.03     | 0.91     | 0.91     | 0.99     | 0.87     | 0.97     | 1.08     | 1.06     | 0.98     |
| MAD$_{VGB}$       | 0.71     | 0.68     | 0.76     | 0.66     | 0.69     | 0.75     | 0.82     | 0.77     | 0.83     | 0.83     |
| AIC$_{LB}$        | 63.32    | 58.92    | 63.56    | 59.75    | 62.27    | 60.78    | 64.06    | 65.83    | 65.05    | 65.06    |
| AIC$_{VGB}$       | 56.25    | 54.16    | 58.63    | 53.95    | 55.01    | 58.27    | 60.86    | 59.48    | 61.25    | 62.86    |
| BIC$_{LB}$        | 67.57    | 63.17    | 67.81    | 64.00    | 66.52    | 65.03    | 68.31    | 70.07    | 69.30    | 69.31    |
| BIC$_{VGB}$       | 61.20    | 59.12    | 63.59    | 58.91    | 59.97    | 63.23    | 65.82    | 64.43    | 66.21    | 67.82    |

https://doi.org/10.1371/journal.pone.0214778.t004
Conclusion

Based on the biological interpretations of parameters and good quality assessors, the VGB model proved superior to the LB one to describe growth curves. The results obtained indicated the VGB model may be an alternative to describe in vitro gas production curves. Therefore, it is recommended for the study of gas production kinetics from forage grasses in genetic enhancement programs according to the methodology and conditions under which the present study was developed.

Supporting information

S1 File. Peanut_rain_data.
(XLSX)

Author Contributions

Conceptualization: Frank Gomes-Silva, Cícero Carlos Ramos de Brito, Luiz Gustavo Ribeiro Pereira.

Data curation: André Luiz Pinto dos Santos, Frank Gomes-Silva, Luiz Gustavo Ribeiro Pereira, Rogério Martins Maurício, José Augusto Gomes Azevêdo, José Marques Pereira, Alexandre Lima Ferreira, Moacyr Cunha Filho.

Formal analysis: André Luiz Pinto dos Santos, Guilherme Rocha Moreira, Frank Gomes-Silva, Cícero Carlos Ramos de Brito, Maria Lindomárcia Leonardo da Costa, Luiz Gustavo Ribeiro Pereira, Rogério Martins Maurício, José Augusto Gomes Azevêdo, José Marques Pereira, Alexandre Lima Ferreira.

Investigation: André Luiz Pinto dos Santos, Guilherme Rocha Moreira, Maria Lindomárcia Leonardo da Costa.

Methodology: André Luiz Pinto dos Santos, Guilherme Rocha Moreira, Frank Gomes-Silva, Cícero Carlos Ramos de Brito.

Software: André Luiz Pinto dos Santos.

Supervision: Guilherme Rocha Moreira, Frank Gomes-Silva, Cícero Carlos Ramos de Brito.

Validation: Guilherme Rocha Moreira.

Writing – original draft: André Luiz Pinto dos Santos, Guilherme Rocha Moreira, Frank Gomes-Silva, Maria Lindomária Leonardo da Costa, Luiz Gustavo Ribeiro Pereira, Rogério Martins Maurício, José Augusto Gomes Azevêdo, José Marques Pereira, Alexandre Lima Ferreira, Moacyr Cunha Filho.

Writing – review & editing: André Luiz Pinto dos Santos, Guilherme Rocha Moreira, Cícero Carlos Ramos de Brito, Maria Lindomária Leonardo da Costa, Rogério Martins Maurício, José Augusto Gomes Azevêdo, José Marques Pereira, Moacyr Cunha Filho.

References

1. JACOVETTI R. Agronomic and nutritional performance of “Mulato II” grass under doses and nitrogen sources. Tese, Goiás Federal University. 2016. https://repositorio.ufg.br/tede/handle/tede/6793

2. MERTENS DR. Rate and extension of digestion. In: FORBES J.M.; FRANCE J. (Eds.). QUALITATIVE ASPECTS OF RUMINANT DIGESTION AND METABOLISM, Cambridge. [Proceedings …]. Cambridge-UK: CAB International; 1993. pp. 13–51.
3. FARIAS LN, VASCONCELOS VR, CARVALHO FFR, SARMENTO JL R. Evaluation of two-compartment logistic and Gompertz mathematical models to estimate gas production from babassu (Orbignya martiana) meal and pie using the semi-automated in vitro technique. Arquivo Brasileiro de Medicina Veterinária e Zootecnia, 2011; 63:136–142.

4. SILVA NA, LIMA RR, SILVA FF, MUNIZ JA. Bayesian hierarchical model applied to genetic evaluation of beef cattle growth curves. Arquivo Brasileiro de Medicina Veterinária e Zootecnia, 2010; 62:409–416.

5. KOOPS WJ. Multiphasic growth curve analysis. Growth, Bar Harbor, 1986; 50:169–177. PMID: 3792903.

6. SCHOFIELD P PITT RE, PELL AN. Kinetics of fiber digestion from in vitro gas production. Journal of Animal Science, Champagne, v. 72. p. 2980–2991, 1994. https://doi.org/10.2527/1994.72112980x

7. FERRO MM, CASTRO WR, ZANINE ADM, SOUZA AL. Kinetics of sugarcane silage with dehydrated barley residue in vitro ruminal fermentation. Archivos de zootecnia, 2017; 66:237–242.

8. PERETTI J, HENRIQUE DS, MAYER LRR, MILITÁO ER, SCHIMITZ R, BOGER DT, et al. Chemical composition and ruminal degradability of white oat (“Avena sativa” L.) cv. IPR126 under different nitrogen levels. Revista Brasileira de Saúde e Produção Animal, 2017; 18:89–102.

9. FRANCE J, DJUKSTRA J, DHANAOA MS, LÓPEZ S, BANNINK A. Estimating the extent of degradation of ruminant feeds from a description of their gas production profiles observed in vitro: derivation of models and other mathematical considerations. British Journal of Nutrition, 2000; 83:143–150. https://doi.org/10.107/S0007114500001180

10. WANG M, TANG SX, TAN ZL. Modeling in vitro gas production kinetics: derivation of logistic–exponential (LE) equations and comparison of models. Animal Feed Science and Technology, 2011; 165:137–150.

11. BRITO CCR, DA SILVA JAA, FERREIRA RLC, DE SOUZA SANTOS E, FERRAZ I. Growth resulting from the variation and combination of models of Chapman; Richards and Silva-Bailey applied to Leucaena leucocephala (Lam.) of Wit. Ciência Florestal, 2007; 17:175–185.

12. SANTANA TJS, SCALON JD, BITTENCOURT TCC, DE SANTANA ASA. A von bertalanffy model with response plateau to describe growth curves of beef cattle. Biometric Brazilian Journal, 2016; 34:646–655.

13. SANTOS ALP, MOREIRA GR, BRITO CCR, SILVA FSG, COSTA MLL, PIMENTEL PG, et al. Method to generate growth and degrowth models obtained from differential equations applied to agrarian sciences. SEMINA. CIÊNCIAS AGRÁRIAS (ONLINE), 2018.

14. ASSOCIATION OF OFFICIAL ANALYTICAL CHEMISTS–AOAC. OFFICIAL METHODS OF ANALYSIS. 15. edition. Arlington, Virginia. 1117p. 1990.

15. VAN SOEST PJ, ROBERTSON JB, LEWIS BA. Methods for dietary fiber, neutral detergent fiber, and nonstarch polysaccharides in relation to animal nutrition. Journal of dairy science, 1991; 74:3583–3597. https://doi.org/10.3168/jds.S0022-0302(91)78551-2 PMID: 1660498

16. MAURÍCIO RM, PEREIRA LGR, GONÇALVES LC, RODRIGUEZ NM, BORGES A, BORGES I, et al. Obtención da equação quadrática entre volume e pressão para a implantação da técnica “in vitro” semi-automática de produção de gás para avaliação de forrageiras tropicales. In: REUNIÃO ANUAL DA SOCIEDADE BRASILEIRA DE ZOOTECNIA, Piracicaba, SP. Anais... Piracicaba, SBZ, 2001; 38:1340–1346.

17. MELLO R, MAGALHÃES ALR, BREnda FC, REGAZZI AJ. Models for fit of gas production in sunflower and corn silages. Pesquisa Agropecuária Brasileira, 2008; 43:261–269.

18. UCKARDES F, EFE E. Investigation on the usability of some mathematical models in in vitro gas production techniques. Slovak Journal of Animal Science, 2014; 47:172–179.

19. ZWIETERING MH, JONGENBURGER I, ROMBOUTS FM, VANT RIET K. Modeling of the bacterial growth curve. Applied and Environmental Microbiology, 1990; 56:1875–1881. PMID: 16348228.

20. PEREIRA MB. Ajustes de modelos à cinética de fermentação em equinos. Dissertação, Federal Rural University of Rio de Janeiro, Seropédica. 2013. http://r1.ufrj.br/wp/pqgz/files/2015/05/Disserta%C3%A7%C3%A3o_-_Marcos_Barreto_Pereira.pdf

21. R Development Core Team. R: A language and environment for statistical computing. Vienna: R Foundation for Statistical Computing, 2017. http://www.r-project.org.

22. CAVALCANTE M, LIRA MDA. Genetic Variability in Pennisetum purpureum Schumacher. Revista Caatinga, Mossoro, 2010; 23:153–163.

23. SCHUNEMANN AP, TREPTOW R, LEITE DL, VENDRUSCOLO JL. Pungência e características químicas em bulbos de genótipos de cebola (Allium cepa L.) cultivados no Alto Vale do Itajai, SC, Brasil. Current Agricultural Science and Technology, v. 12, n. 1, 2006; 12:77–80.
24. FERREIRA AL, MAURICIO RM, PEREIRA LGR, AZEVEDO JAG, OLIVEIRA LS, PEREIRA JM. Nutritional divergence in genotypes of forage peanut. Revista Brasileira de Zootecnia, 2012a; 41:856–863.

25. FERREIRA AL, MAURICIO RM, FERNANDES FD, CARVALHO MA, RAMOS AKB, JUNIOR RG. Ranking contrasting genotypes of forage peanut based on nutritive value and fermentation kinetics. Animal feed science and technology, 2012b; 175:16–23.

26. ARAGA-DAY-YUNGÁN RG, RAYAS AMOR AA, HEREDIA-NAVÁ D, ESTRADA-FLORES JG, MARTÍNEZ-CASTAÑEDA FE, ARRIAGA-JORDÁN CM. Evaluación in vitro del ensilaje de girasol (Helianthus annuus L.) solo y combinado con ensilaje de maíz. Revista Mexicana de Ciencias Pecuarias, Instituto Nacional de Investigaciones Forestales, Agrícolas y Pecuarias, México, 2015, 6: 315–327.

27. SÁ JF, PEDREIRA MS, SILVA FF, FIGUEIREDO MP, REBOUÇAS GMN, DE SOUZA DR. Cinética da fermentação in vitro do capim-Marandu em diferentes idades de corte. Acta Scientiarum Animal Sciences. 2011; 33:225–231.

28. DOS ESL, RUFINO LD, RIBEIRO KG, PEREIRA OG. Microbial characterization of Arachis pintoi and its silages at different fermentation periods. Molecular biology reports. 2019. https://doi.org/10.1007/s11033-019-04952-y

29. NOGUEIRA UT, MAURICIO RM, GONÇALVES LC. Comparison among substrates with different soluble carbohydrates concentration using the in vitro semi-automatic gas production technique. Archivo Brasileiro de Medicina Veterinaria e Zootecnia, 2006; 58:633–641 http://dx.doi.org/10.1590/S0102-09352006000400027

30. DA SILVA AL, DE SOUSA DB, AMORIM DS, DA SILVA SANTOS M, DA SILVA KB, DO NASCIMENTO RR. Carbohidratos de plantas forrageiras para ruminantes: importância e avaliação qualitativa: uma revisão. Nucleus Animalium. 2019; 11:1–12. http://dx.doi.org/10.3738/21751463.2945.

31. CABRAL LS, VALADARES FILHO SC, MALAFIA PAM, LANA RP, SILVA JFC, VIEIRA RAM, et al. Forage Carbohydrate Fractions and its Degradation Rates Estimated by Gas Production Technique. Revista Brasileira de Zootecnia, 2000; 29:2087–2098.

32. MALAFIA PAM, VALADARES FILHO SDC, VIEIRA RAM, SILVA JD, PEREIRA JC. Ruminal Kinetics of Some Feeds Investigated by Gravimetric and Metabolic Techniques. Revista Brasileira de Zootecnia. 1998; 27:370–380.

33. RICACHEKSI ST, HENRIQUE DS, MAYER LRR, OLIVEIRA JG, ROSLER JA, FLUCK AC. Chemical composition and ruminal degradation kinetics of white oat (Avena sativa L.) IPR 126. Revista Brasileira de Saúde e Produção Animal, 2017; 18:50–61.

34. KRISHNAMOORTHY U, RYMER C, ROBINSON PH. The in vitro gas production technique: Limitations and opportunities. Animal Feed Science and Technology, 2005; 123–124:1–7.

35. ARRE FA, CAMPELO JEG, SARMENTO JLR, FIGUEIREDO FILHO LAS, CAVALCANTE DH. A comparison of nonlinear models for describing weight-age data in anglo-nubian does. Revista Caatinga, 2019; 32: 251–258.

36. SILVEIRA FGD, SILVA FF, CARNEIRO PL, MALHADO CHM, MUNIZ JA. Cluster analysis applied to nonlinear regression models selection to growth curves of crossed lambs. Ciência Rural, 2011; 41:692–698.

37. SILVEIRA FG, SILVA FF, CARNEIRO PL, MALHADO CHM, PETERNELLI LA, SOUZA JR AAO. Classificação multivariada de modelos de crescimento para grupos genéticos de ovinos de corte. In: 54ª RBRAS (Reunião Anual da Região Brasileira da Sociedade Internacional de Biometria) e 13ª SEAGRO (Simpósio de Estatística Aplicada à Experimentação Agronômica), 2009, São Carlos-SP. Anais da 54ª RBRAS e 13ª SEAGRO. São Carlos-SP: UFS/C, 2009.

38. GONDIM FILHO AGC. Genetic divergence and evaluation of degradation models in forage peanut genotypes (Arachis pintoi). Thesis, Federal Rural University of Pernambuco. 2018. http://www.tede2.ufpe.br:8080/tede2/handle/tede2/71239

39. GROOT JC, CONE JW, WILLIAMS BA, DEBERSAQUES FMA, LANTINGA EA. Multiphasic analysis of gas production kinetics for in vitro fermentation of ruminant feeds. Animal Feed Science and Technology, 1996; 64:77–89.