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This is the author's accepted version of the contribution published as:

Original
Quantitative Scaling of Magnetic Avalanches / Durin, Gianfranco; Bohn, F; Corrêa, M. A; Sommer, R. L; Le Doussal, P; Wiese, K. J.. - In: PHYSICAL REVIEW LETTERS. - ISSN 0031-9007. - 117:8(2016), p. 087201. [10.1103/PhysRevLett.117.087201]

Availability:
This version is available at: 11696/53365 since: 2016-11-28T14:49:27Z

Publisher:
APS

Published
DOI:10.1103/PhysRevLett.117.087201

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Quantitative scaling of magnetic avalanches

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We provide the first quantitative comparison between Barkhausen noise experiments and recent predictions from the theory of avalanches for pinned interfaces, both in and beyond mean-field. We study different classes of soft magnetic materials: polycrystals and amorphous samples, characterized by long-range and short-range elasticity, respectively; both for thick and thin samples, i.e. with and without eddy currents. The temporal avalanche shape at fixed size, and observables related to the joint distribution of sizes and durations are analyzed in detail. Both long-range and short-range samples with no eddy currents are fitted extremely well by the theoretical predictions. In particular, the short-range samples provide the first reliable test of the theory beyond mean-field. The thick samples show systematic deviations from the scaling theory, providing unambiguous signatures for the presence of eddy currents.

PACS numbers: 89.75.Da, 75.60.Ej, 75.60.Ch, 75.70.Ak

Barkhausen noise in soft magnets originates from the jerky motion of magnetic domain walls (DWs), and is characterized by scale-free power-law distributions of magnetization jumps [1–5]. It is the earliest and most scrutinized probe for avalanche motion, an ubiquitous phenomenon present in other systems such as fluid contact-line depinning [8, 9], brittle fracture fronts [10, 11], and pinned vortex lines [12]. In all these systems the motion of an overdamped elastic interface (of internal dimension \(d\)) driven in a quenched medium was proposed as an efficient mesoscopic description. However, until now, analytical predictions, allowing for a detailed comparison with experiments, have been scarce, due to the difficulty in treating collective discontinuous jumps in presence of many metastable states.

Toy models have thus been developed, capturing essential features at the level of mean-field (MF). One celebrated example is the ABBM model, where the domain wall is modeled as a single point in an “effective” random force landscape performing a (biased) Brownian motion [13–15]. Refinements based on infinite-range models were later proposed [16], leading to similar physics [15, 17]. These MF toy models predict an avalanche-size distribution \(P(S) \sim S^{-\tau} \propto S^{-\mu} \sim \mu \sim 3/2\) and a duration distribution \(P(T) \sim T^{-\alpha} \sim T^{-\mu} \sim 2\) with \(\alpha = \alpha_{MF} = 2\).

The theory of interface depinning provides a predictive universal framework for the avalanche statistics. It involves two independent exponents, the roughness exponent \(\zeta\) and the dynamical exponent \(z\). The distribution exponents \(\alpha\) and \(\tau\) were conjectured from scaling, as in the Narayan-Fisher (NF) conjecture \(\tau = 2 - \frac{\mu}{\alpha + \zeta - \mu}\) and \(\alpha = \alpha = 1 + \frac{d + \zeta - \mu}{z}\), where \(\mu\) describes the range of interactions. The upper-critical dimension at which \(\zeta = 0\) and below which mean-field models fail is \(d_{uc} = 4\) for short-range elasticity (SR, \(\mu = 2\)) and \(d_{uc} = 2\) for long-range elasticity (LR, \(\mu = 1\)) [17].

In Barkhausen noise experiments, two distinct families of samples were identified, consistent with these predictions [4]. In polycrystalline materials, the DW experiences strong anisotropic crystal fields leading to LR elasticity. In the \(D = d + 1 = 2 + 1\) geometry this system behaves according to MF theory. In amorphous samples, SR elasticity prevails over a negligible LR elasticity, and the avalanche exponents agree with the NF prediction. In both cases, a relevant role is played by the demagnetizing field, which acts as a cutoff for large avalanches [4]. These mean-field predictions were tested in soft magnetic thin films, where the retarding effects of eddy currents (ECs) of bulk samples are negligible [5].

Recently, it became possible to compare theory and experiments of avalanches well beyond scaling and the value of exponents. On the theoretical side, the functional renormalization group of depinning was extended to calculate a host of avalanche observables [6, 7, 21–24]. Examples are the avalanche shape at fixed size and duration, the joint size distribution, both in mean-field and beyond, even including retardation effects due to eddy currents [20]. On the experimental side, the avalanche shape was studied in magnetic systems [5, 7], in fracture and imbibition [25]. Despite these experiments, most of the recent predictions of the theory have not yet been tested quantitatively, especially not to high accuracy.

The aim of this Letter is to provide new and sensitive tests of these theoretical predictions in soft ferromagnets. This is possible since in our Barkhausen experiment we detected a high number of avalanches, getting a robust statistics. Diverse magnetic samples have been explored, corresponding to the two universality classes (LR and SR), with and without EC effects. We focus our atten-
Figure 1. Normalized average size \( \langle S \rangle_T / S_m \) of Barkhausen avalanches in the FeSi ribbon (blue dots) and the Py thin film (red dots) as a function of the normalized duration \( T = T / \tau_m \). The continuous line is the theoretical prediction \( g_1^{MF} \) of Eq. \( \{1\} \). For the ribbon, the deviation at large durations is more evident due to effect of the eddy currents. The inset shows the second moment \( \langle S^2 \rangle_T / S_m^2 \) compared to the prediction \( g_2^{MF} \) of Eq. \( \{1\} \).

Figure 2. Normalized average size \( \langle S \rangle_T / S_m \) of avalanches in the FeCoB ribbon (blue dots) and the FeSiB thin film (red dots) as a function of \( T / \tau_m \). The continuous line is the theoretical prediction of Eq. \( \{5\} \), with \( \epsilon = 2 \), so that \( \langle S \rangle_T / S_m \sim 0.528 \left( T / \tau_m \right)^{\gamma} \), with \( \gamma \approx 1.76 \). The ribbon shows a larger deviation due to eddy currents. A comparison with the expected linear behavior at large \( \tilde{T} \) is indicated by the dashed line. Remarkably, this deviation occurs at sizes larger than the size cutoff \( 4 S_m \), i.e. for \( \langle S \rangle_T / S_m > 4 \).

The simplest observables we can consider are the moments of the average size at fixed duration

\[
\langle S^n \rangle_T = (S_m)^n g_n(T/\tau_m), \quad g_n(\tilde{T}) \sim_{\tilde{T} \to 0} c_n \tilde{T}^{n\gamma},
\]

whose universal behavior for small avalanches defines the exponent \( \gamma \). Here, \( \tilde{T} = T / \tau_m \) is the rescaled avalanche duration. In mean-field, one finds

\[
\gamma^{MF} = 2, \quad c_1^{MF} = \frac{1}{3}, \quad c_2^{MF} = \frac{2}{15},
\]

and the scaling functions are

\[
g_1^{MF}(\tilde{T}) = 2 \tilde{T} \coth(\tilde{T}/2) - 4, \tag{4}
g_2^{MF}(\tilde{T}) = 2 \tilde{T} \csch^2\left(\frac{\tilde{T}}{2}\right) \left[ \tilde{T} (\cosh(\tilde{T}) + 2) - 3 \sinh(\tilde{T}) \right].
\]

Beyond mean-field, one finds

\[
\gamma = \frac{d + \zeta}{z}, \quad c_1 = c_1^{MF} + \frac{11 - 3 \gamma E - \ln 4}{81} \epsilon, \tag{5}
\]

where the expression for \( c_1 \) has been calculated to first order in \( \epsilon = d_{we} - d \). This leads to \( c_1 \approx 0.528 \) for \( \epsilon = 2 \), as in the case of \( \mu = 2 \) and \( d = 2 \) (\( \gamma_E \approx 0.577 \)).

Another observable of interest is the averaged avalanche duration at fixed size. In mean field, it is given by

\[
\langle T \rangle_{S/\tau_m} = \sqrt{\pi S / S_m}, \tag{6}
\]
which is consistent with the general expected scaling \( (T)_S \sim S^{1/\gamma} \), with \( \gamma = \gamma_{\text{MF}} \). Remarkably, within mean-field, Eq. (4) holds for any value of the ratio \( S/S_m \).

Let us now consider the average temporal avalanche shape at fixed size, \( \langle \dot{u}(t) \rangle_S \), which takes the form

\[
\langle \dot{u}(t) \rangle_S = \left( \frac{S}{S_m} \right)^{-\frac{1}{\gamma}} f \left( \frac{t}{\tau_m} \left( \frac{S}{S_m} \right)^{\frac{1}{\gamma}} \right),
\]

where \( f(t) \) is a universal scaling function, and \( \int_0^\infty dt f(t) = 1 \). In mean field, \( f(t) \) is independent of \( S/S_m \) and reads

\[
f_{\text{MF}}(t) = 2te^{-t^2}. \tag{8}
\]

Beyond MF, the function \( f(t) \) has been obtained to \( \mathcal{O}(\varepsilon) \) for SR elasticity. Here, we use the convenient form

\[
f(t) \approx 2te^{-C't} B \exp \left( -\frac{\varepsilon}{\tau_m} \left( \frac{\delta f(t)}{f_{\text{MF}}(t)} - t^2 \ln(2t) \right) \right), \tag{9}
\]

where the function \( \delta f(t) \) is displayed in Eq. (34) of Ref. [24] and \( B \) chosen s.t. \( \int_0^\infty dt f(t) = 1 \), an approximation exact to \( \mathcal{O}(\varepsilon) \). Eq. (9) has asymptotic behaviors

\[
f(t) \simeq_{t \to 0} 2A\tau^{\gamma-1}, \tag{10}
\]

\[
f(t) \simeq_{t \to \infty} 2A't^\beta e^{-C't^4}, \tag{11}
\]

with \( A = 1 + \frac{\varepsilon}{9}(1 - \gamma_E) \), \( A' = 1 + \frac{\varepsilon}{36}(5 - 3\gamma_E - \ln 4) \), \( \beta = 1 - \varepsilon/18 \), \( C = 1 + \frac{\varepsilon}{5} \ln 2 \), and \( \delta = 2 + \varepsilon/9 \).

To compare these theoretical predictions to our experimental results, we first need to make use of dimensionless units, thus rescaling sizes and durations by \( S_m \) and \( \tau_m \), respectively. The parameter \( S_m \) is analytically defined by Eq. (4); we tested that it leads to a consistent comparison of the measured size distribution \( P(S) \) with the theory, see Supplemental Material [22]. In particular, we verified that the cutoff occurs at \( 4S_m \), as predicted. On the other hand, \( \tau_m \) can only be inferred using (i) the expression of Eqs. (2) and (3); and (ii) the data of the average shape \( \langle \dot{u}(t) \rangle_S \). In absence of ECs, the estimation of \( \tau_m \) is made by matching both kind of data with the analytical expressions, giving a consistent and robust estimation of the parameter [24]. In presence of ECs, we use the procedure (i) to estimate \( \tau_m \).

We analysed the avalanche statistics in different classes of materials. Two of them are thin films with negligible eddy current effects: a LR polycrystalline Ni_{81}Fe_{19} Permalloy (Py) with a thickness of 200 nm (\( \tau_m = 39 \mu s \)) and a SR amorphous Fe_{75}Si_{15}B_{10} (FeSiB) alloy, with a thickness of 1000 nm (\( \tau_m = 38 \mu s \)) [1, 2]. The other two samples are ribbons with a thickness of about 20 \( \mu m \), where eddy current retarding effects are well known: a LR polycrystalline FeSi alloy with Si=7.8\%, (\( \tau_m = 2 \) ms), and a SR amorphous Fe_{64}Co_{21}B_{15} (FeCoB) alloy, measured under a small tensile stress of 2 MPa (\( \tau_m = 0.5 \) ms) [3, 4]. All samples have a space dimension \( D = 2 + 1 \); the two LR materials show MF exponents, while the other ones have NF exponents, with \( \varepsilon = 2 \). Further details on the samples and the experiments are given in the Supplemental Material [22].

Figures [1] and [2] report the average size as a function of avalanche duration for LR and SR samples, respectively, compared to the theoretical prediction of Eqs. (4) and (5). In the absence of eddy currents, the correspondence is almost perfect, except for the highest \( (S,T) \) values. For LR samples (Fig. [4]), the mean-field prediction [4] crosses over from \( \sim T^2 \) to \( \sim T \) at large avalanche sizes, a trend which seems to agree with our data.

\[\text{Figure 3. Normalized average duration } (T)_S/\tau_m \text{ of avalanches in the FeSi ribbon (blue dots) and the Py thin film (red dots) as a function of the normalized size } S/S_m. \text{ The continuous line is the theoretical prediction of Eq. (4).}\]

\[\text{Figure 4. Scaling collapse of the average shapes at fixed avalanche sizes } \langle \dot{u}(t) \rangle_S, \text{ according to Eq. (7), in the Py thin film. The continuous line is the mean-field universal scaling function in Eq. (8).}\]
is often argued that a linear dependence can also arise from the superposition of a multiplicity of active DWs. Indeed some of the largest avalanches are a superposition of smaller avalanches occurring in different parts of the sample, triggered by the relatively large change of the magnetization \[S > S_m\]. Furthermore, the retarding effect of eddy currents makes large avalanches (say, for \(S > S_m\)) even longer, so that the average size further deviates from the theoretical prediction, especially in samples with more EC, as seen from Fig. 1. Note that the agreement with the MF predictions is also quite good at the level of fluctuations (i.e., the second moment \((S^2)_T\) in the inset of Fig. 1). For the SR samples in Fig. 2, we plot the prediction for small \(T\), in good agreement with the data up to the size cutoff \(4S_m\), i.e., \((S)_T/S_m \sim 4\). At large \(T\) we expect a similar bending to a linear behavior, although there are presently no detailed predictions for the crossover.

The mean avalanche duration at fixed size, \(\langle T \rangle_S\), is shown in Fig. 3 for LR samples. For the film, it shows an almost perfect agreement with the MF prediction of Eq. [3], indicating that ECs are indeed negligible, while the effect of ECs is clearly visible in the ribbon.

Collapsing the experimental data of the average shapes at fixed size \(\langle \dot{u}(t) \rangle_S\) gives an alternative powerful way to estimate the exponent \(\gamma\), as reported in Figs. 4 and 5. Here we obtain the same exponents as from the average size measurements \((S)_T\), i.e., \(\gamma = 2\), and \(\gamma = 1.76\), for LR and SR respectively. The collapsed average shapes correspond remarkably well to the theoretical predictions of Eqs. [8] and [9], including the behavior in the tails (shown in the SR case in the insets of Fig. 5). In the Supplemental Material [32], we further verify that neither the collapse, nor the quantitative fit can be achieved using the MF prediction.

Finally, it is well known that relaxation of eddy currents introduces a slow time scale into the dynamics, stretching avalanches in time [20]. In Fig. 6 we have obtained an approximate collapse for the SR case in presence of eddy currents, using the theoretical value of \(\gamma = 1.76\). It is a manifest that the resulting curve is different from the one predicted in absence of retardation effects. Hence, this is another unambiguous method to detect the presence of ECs, similarly to the leftward asymmetry of the temporal avalanche shapes at fixed durations [4]. To go further and obtain predictions for the average shape in presence of ECs is difficult, as the shape strongly depends on the detailed parameters of the eddy currents. A step in that direction was obtained within MF in Ref. [20] for a particular model of retardation. Detailed comparison with experiments involve non-universal scales, and is left for a future publication.

In conclusion we have shown how the data from Barkhausen noise experiments can be analyzed and confronted to the most precise recent theoretical predictions. This provides very quantitative and fundamental tests of the theory of avalanches beyond scaling exponents. The prediction of universality will also lead to a better characterization of magnetic systems, allowing to measure its dimensionality and, via the deviations from the theory, effects of multiple avalanches or eddy currents.

This work was supported by PSL grant ANR-10-IDEX-0001-02-PSL and CNPq (Grants No. 306423/2014-6, No. 471302/2013-9, No. 306362/2014-7, and
We acknowledge hospitality of the KITP with support in part by the National Science Foundation under Grant No. NSF PHY11-25915.

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Supplemental material of
Quantitative scaling of magnetic avalanches
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In this supplemental material, we

(A) Provide information on the investigated samples and details on the experiments;

(B) Further characterize the samples, and discuss distributions of avalanche sizes and universality classes;

(C) Provide additional comparison of the data with the theoretical mean-field predictions.

A. Samples and experiments

We employ thin films and ribbons to perform Barkhausen noise experiments.

The thin films correspond to a polycrystalline Ni$_{81}$Fe$_{19}$ Permalloy (Py) film with thickness of 200 nm and an amorphous Fe$_{75}$Si$_{15}$B$_{10}$ (FeSiB) film with the thicknesses of 1000 nm. The films are deposited by magnetron sputtering onto glass substrates, with dimensions 10 mm × 1000 nm. The films are deposited by magnetron sputtering using a 65 W RF power supply. During the deposition, the substrate moves at constant speed with current of 50 mA, while the ferromagnetic layers are deposited using a 2 nm thick Ta buffer layer. The Ta layer is deposited using a DC source with a constant magnetic field of 1 kOe is applied along the main axis of the substrate in order to induce magnetic anisotropy. Detailed information on the structural and magnetic characteristics is found in Refs. [1, 2].

The ribbons are a polycrystalline FeSi alloy with Si=7.8% and an amorphous Fe$_{64}$Co$_{21}$B$_{15}$ (FeCoB), both with thickness of about 20 µm. The experiments are performed with ribbons of dimensions of about 20 cm × 1 cm, and the FeCoB one is measured under a small tensile stress of 2 MPa in order to enhance the signal-to-noise ratio. Further information on the ribbons is found in Refs. [3, 4].

We record Barkhausen noise time series using the traditional inductive technique in an open magnetic circuit, in which one detects time series of voltage pulses with a sensing coil wound around a ferromagnetic material submitted to a slow-varying magnetic field. In our setup, the sample and pick up coils are inserted in a long solenoid with compensation for the borders, to ensure an homogeneous applied magnetic field on the sample. The sample is driven by a triangular magnetic field, applied along the main axis of the sample, with an amplitude high enough to saturate it magnetically. Barkhausen noise is detected by a sensing coil wound around the central part of the sample. A second pickup coil, with the same cross section and number of turns, is adapted in order to compensate the signal induced by the magnetizing field. The Barkhausen signal is then amplified, filtered, and finally digitalized. For the thin films, Barkhausen noise measurements are performed using a sensing coil with 400 turns, 3.5 mm long and 4.5 mm wide, and under similar conditions, i.e., 50 mHz triangular magnetic field, 100 kHz low-pass filter set in the preamplifier and signal acquisition with sampling rate of 4 × 10$^6$ samples per second [1, 2]. For the ribbons, the experiments are carried out using a sensing coil with 50 turns, 1 mm long and 1 cm wide, triangular magnetic field with frequency of 3-5 mHz, and low pass preamplifier filter chosen in the 3-20 kHz range, roughly half of the sampling rate [3, 4].

All the time series are acquired just around the central part of the hysteresis loop, near the coercive field, where the domain wall motion is the main magnetization mechanism [3]. For each experimental run, the statistical properties are obtained from at least 150 measured Barkhausen noise time series.

B. Distribution of avalanche sizes

Here, we further characterize the investigated samples and show why they belong to different universality classes. Figure S2 presents the distributions of avalanche sizes P(S) for the LR and the SR samples. All the distributions follow a cutoff-limited power-law scaling behavior, as expected. The LR samples, i.e. the polycrystalline Py thin film and FeSi ribbon, are characterized by mean-field exponent, $\tau \sim 1.5$, and well described by the theoretical prediction $P(S) = S^{-\tau_0} \exp(-S/S_m)$ of Ref. [6]. Due to finite rate effects, the experimental exponents are a little smaller than the prediction, although the cutoff of the prediction is perfectly predicted at $4S_m$. The SR samples, i.e. the FeSiB thin film and the FeCoB ribbon, present the Narayan-Fisher exponent $\tau = 1.26$, and are well described by the theoretical prediction of Ref. [7], Eqs. (169)-(172), in which $P(S) = S^{-\tau} \exp(C\sqrt{S/S_m} - B(S/4S_m)^{\delta})$, with $B = 1 + \alpha(1 + \gamma_E/4)$, $C = 1/2\sqrt{\tau_0}$, $\alpha = 1/3(1 - \zeta_1)\epsilon$, $\delta = 1 + \epsilon/18$, where $\zeta_1 = 1/3$ and $\epsilon = d_{\text{uc}} - d = 2$.

C. Additional comparison with mean-field predictions

The aim of this section is to show that the data for the SR samples cannot be fit consistently with the mean-field predictions.

Let us start with the average normalized size $\langle S \rangle_T/S_m$ as a function of the normalized duration $\tilde{T} = T/\tau_m$. When compared with the MF prediction $g_{\text{MF}}(\tilde{T}) = \epsilon^\tau T^{\frac{\alpha}{\gamma_E}} \exp(-\frac{\alpha}{\gamma_E} T^{\frac{1}{\gamma_E}})$, the experimental data are quite well described by $g(\tilde{T}) = \epsilon^\tau T^{\frac{\alpha}{\gamma_E}} \exp(-(1 - \zeta_1)\epsilon T^{\frac{1}{\gamma_E}})$. This is in agreement with the theoretical prediction of Ref. [7], Eqs. (169)-(172), and with the analysis of Ref. [8]. The deviations from MF scaling are mainly due to finite rate effects.
Figure S1. Average sizes $\langle S \rangle_T / S_m$ of avalanches in the SR samples, FeCoB ribbon (blue dots) and the FeSiB thin film (red dots). The dash lines are the theoretical MF prediction $g_{1}^{MF}(T) = 2\tilde{T} \coth(\tilde{T}/2) - 4$, for two different values of $\tau_m$.

Figure S2. Left: Distributions of avalanche sizes $P(S)$ in MF samples, the FeSi ribbon (blue dots) and the Py thin film (red dots). The continuous line is the theoretical prediction $P(S) = S^{-\gamma} \exp\left(S/4S_m\right)$ of Ref. [6]. Here, $\tau$ is a little smaller of the adiabatic value of 1.5 because of the finite rate effects [5]. On the other hand, the cutoff of the distribution is perfectly predicted at $4S_m$. Right: $P(S)$ of SR samples, the FeCoB ribbon (blue dots) and the FeSiB thin film (red dots). The continuous line is the theoretical prediction of Ref. [7], Eqs. (169)-(172), in which $P(S) = S^{-\gamma} \exp\left(C\sqrt{S/S_m} - B(S/4S_m)^{\delta}\right)$, with $\tau = 1.26$, $B = 1.51$, $C = 0.34$, and $\delta = 1.11$.

2$\tilde{T} \coth(\tilde{T}/2) - 4$, we need to adapt the value of the $\tau_m$, as explained in the main paper. Here we need to increase its value by 30% (see Fig. S1 left) up to 50% (right) compared to the value of Fig. 2 of the paper. It is clear that the MF curve, having $\gamma = 2$, larger than the experimental data, either follows low value data but fails for the higher ones or intersects them at some point. In practice, it cannot correctly describe the experiments.

Let us now discuss the data for the avalanche shapes.

The main question is whether the data for the SR samples can be fitted by the MF predictions, which means (i) $\gamma = 2$, and (ii) a scaling function $f(t) = f_{MF}(t) = 2te^{-t^2}$.

In Fig. S3 (left) we present the data rescaled with the choice $\gamma = 2$. Obviously there is no data collapse for various sizes. This feature is clearly independent of the choice of $\tau_m$ as depends on $\gamma$ only. This rules out the MF prediction to compare with the data.

Another question, mostly of theoretical interest, is how the scaling function of the rescaling of the data with $\gamma \sim 1.76$ in Fig. 5 of the main paper differs quantitatively from the MF prediction $f_{MF}(t)$. In Fig. S3 (right) to compare the two curves we need to artificially change
the $\tau_m$ value, which is smaller and incompatible with the values of Fig. S1. More striking, the scaling function is linear at low values, while the data follow a $t^{\gamma-1}$ law.

In conclusion, it is important to emphasize that a quantitative comparison of the experimental data with the theoretical predictions is only possible when the values of the parameters $\gamma, \tau_m, S_m$ are fixed, and compatible with the theoretical curves. In other words, a single visual comparison may not be enough to establish the universality class. Here we demonstrated that the use of at least two independent measurements (such as the average size, and the average shapes at fixed sizes) set constrains that unambiguously determine the universality class. This is particularly important when applied to other systems showing a similar crackling noise, or in more general displaying a dynamical phase transition.

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