VO₂ Carbon Nanotube Composite Memristor-Based Cellular Neural Network Pattern Formation

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Abstract: A cellular neural network (CNN) based on a VO₂ carbon nanotube memristor is proposed in this paper. The device is modeled by SPICE at first, and then the cell dynamic characteristics based on the device are analyzed. It is pointed out that only when the cell is at the sharp edge of chaos can the cell be successfully awakened after the CNN is formed. In this paper, we give the example of a 5 × 5 CNN, set specific initial conditions and observe the formed pattern. Because the generated patterns are affected by the initial conditions, the cell power supply can be pre-programmed to obtain specific patterns, which can be applied to the future information processing system based on complex space–time patterns, especially in the field of computer vision.

Keywords: VO₂ carbon nanotube composite memristor; cellular neural network (CNN); von Neumann structure; local activity; edge of chaos

1. Introduction

The traditional processor uses the von Neumann structure, in which the storage unit and the processing unit are separated and connected by bus. In recent years, with the development of semiconductor technology, the speed of processing units has been greatly improved. However, due to the limitation of bus bandwidth, the operation speed of the whole processor is limited, which is called the “von Neumann bottleneck problem” [1,2]. In order to solve this problem, inspired by the biological way of processing information, many pieces of literature have proposed various non-von Neumann processor solutions [3–5]. Typical bio-inspired computing relies on nonlinear networks that contain the same cells; each cell has a relatively simple structure and interacts with the surrounding cells. This structure, called a CNN, a cellular neural network, has been applied in fields such as computer vision [6–8].

The concept of a CNN can be traced back to two articles by Chua in 1988 [9,10], which respectively give the theory and application of CNNs. Recently, Itoh [11] summarized some characteristics of CNNs in a long paper. Weiher et al. [12] discussed the pattern formation of CNNs based on the NbO₂ memristor.

Recently, brain-like computing has become a hot topic in research [13–15], and the key is to find devices that can produce spike signals like neurons and that have very low power consumption. The VO₂ carbon nanotube (CNT) composite device is a Mott memristor recently proposed [16]. It can generate periodic peak pulses with a pulse width of less than 20 ns, it is driven by a DC current or voltage, and it does not need additional capacitance. It uses metal–carbon nanotubes as heaters, and, compared with the pure Mott VO₂ proposed earlier, adding CNTs can greatly reduce the transient duration and pulse energy and increase the frequency of a peak pulse by three orders of magnitude.

The VO₂ nano crossbar device does not need the process of electric forming and has low device size dispersion. For devices with a critical size between 50 and 600 nm, the change coefficient of the switch threshold voltage is less than 13%, the switch durability is more than 26.6 million cycles, and the IV characteristics of the device are not changed...
significantly. The VO$_2$ device technology in the process of non-electric formation accelerates the development of an active memristor neuron circuit. It can simulate the most known neuron dynamics and clear the way for the realization of a large-scale integrated circuit (IC). In addition, the VO$_2$ memristor is superior to its NbO$_2$ counterpart in both switch speed and switching energy. The simulated Mott transition in the VO$_2$ is 100 times faster than in the NbO$_2$ and consumes only about one-sixth (16%) of the energy [17].

In this paper, a cellular neural network based on a VO$_2$ CNT is proposed. As a cell itself, a VO$_2$ CNT is set to be stable and static, that is, in “sleep”. If the memristor is on the “edge of chaos”, two or more cells are connected by the RC coupling, which will make it in the state of “wake-up”, namely, in the dynamic oscillation mode. The second part of this paper is the modeling of VO$_2$ CNT composite devices, providing the SPICE model. The third part is the cell circuit, which gives the analysis process of the decoupled circuit. The response of the memristor is expanded near the operating point and the small-signal equivalent circuit is given. Based on this, the influence of coupling $R$ and $C$ device parameters on the input impedance of one port is analyzed. The fourth part is the CNN simulation, which describes the pattern formation characteristics of a CNN composed of memristor-based cells.

Compared with the traditional CMOS realization of CNN, the memristor counterpart can largely save power and chip area, and provide ultra-high processing speeds.

2. VO$_2$ Carbon Nanotube Composite Device Modeling

The structure of the VO$_2$ carbon nanotube composite device is shown in Figure 1. It contains a transverse active region, which is defined by a VO$_2$ thin metal strip with a thickness of about 5 nm (as shown in the red region of the figure), and its two ends are connected with Pd electrodes (as shown in the blue region of the figure). This is a planar Mott metal-insulator transition device. The aligned carbon nanotubes (as shown in the black line) were first grown on quartz substrate, and then transferred to the surface of a VO$_2$ thin metal strip before the whole device was formed.

![Figure 1. A VO$_2$ carbon nanotube composite device structure. The red part is the VO$_2$ and the black line over it represents the carbon nanotube.](image)

As a Mott metal-insulator transition device, it satisfies the following equation [16]:

$$i_m = \frac{dT}{dt} = \frac{A T^2 e^{\beta \phi/m-kT}}{C_{th}} = \frac{T-T_{amb}}{C_{th}R_{th}}$$

The first formula of Equation (1) is the current emission equation of the Schottky diode, and the second formula is Newton’s cooling law, where, $i_m$ and $\gamma_m$ are the current and voltage through the memristor NDR device, respectively; $T$ is the absolute temperature of the device; $T_{amb}$ is the ambient temperature; $A$ and $\beta$ are scaling constants; $d$ is the effective device length; $k$ is Boltzmann constant; $\phi$ is the energy barrier; $C_{th}$ is the heat capacity (effective thermal mass); $R_{th}$ is the thermal resistance; $R_{CNT}$ is the resistance value of the CNT (carbon nanotube), taking 600 kΩ. The second expression of Equation (1) represents the electrical and thermal coupling between $R_{CNT}$ and VO$_2$. The parameters of the device are shown in Table 1.
Table 1. Device parameters. The data is cited directly from the literature [16].

| Parameter      | VO₂ CNT Device |
|----------------|----------------|
| $T_{\text{amb}}$ | 296 K          |
| $\beta$        | $3.3 \times 10^{-4} \text{ eV} \cdot \text{m}^{0.5} \cdot \text{V}^{-0.5}$ |
| $A$            | $1.7 \times 10^{-8} \text{ A} \cdot \text{K}^{-2}$ |
| $d$            | $5 \times 10^{-6} \text{ m}$ |
| $R_{\text{th}}$ | $2.5 \times 10^{9} \text{ K} \cdot \text{W}^{-1}$ |
| $C_{\text{th}}$ | $5 \times 10^{-17} \text{ J} \cdot \text{K}^{-1}$ |
| $R_{\text{S}}$ | 5500 $\text{Ω}$ |
| $V_{\text{S}}$ | 10 $\text{ V}$ |
| $R_{\text{CNT}}$ | 600,000 $\text{Ω}$ |
| $\phi$         | 0.58 $\text{eV}$ |
| $k$            | $8.62 \times 10^{-5} \text{ eV} \cdot \text{K}^{-1}$ |

According to Equation (1), the SPICE model of the device can be established, as shown in Figure 2.

![Figure 2. SPICE model of the device.](image)

The quasi-static volt-ampere characteristics of the device can be obtained by using the SPICE model, as shown in Figure 3.

![Figure 3. Quasi-static volt-ampere characteristics of the VO₂ carbon nanotube composite device.](image)

The simulation measurement method of the quasi-static volt-ampere characteristics of the device is to use a sinusoidal voltage source with a frequency of 1 Hz and amplitude of 10 $\text{V}$ to excite the device through a small series resistor, and then draw the V–I relationship...
curve by measuring the current flowing through the device. When you look at Figure 3, you can clearly see a hysteresis region, which is a typical feature of the local active memristor.

3. Cell Circuit

Figure 4 is the designed circuit of a memristor cell, in which $R_S$ is the bias resistor, $M$ is the VO$_2$ memristor and $R_{CNT}$ is the carbon nanotube resistance. The parallel resistor and capacitor combination is the circuit coupled with adjacent cells, and it is also a part of the cell.

According to Figure 4, the circuit equation can be obtained by using the Kirchhoff current law, the Kirchhoff voltage law and Equation (1), as follows:

$$\frac{dT}{dt} = \frac{v_m + v_m^2 / R_{CNT}}{C_{th}} - \frac{T - T_{amb}}{C_{th} R_{th}}$$

$$C \frac{dv_C}{dt} = -\frac{v_C}{R} + i_A$$

$$0 = -i_m + AT^2 e^{\frac{v_m}{d} - \phi}$$

$$0 = -V_S + R_S i_m + (1 + R_S/R_{CNT})v_m - R_S i_A$$

$$v_A = v_C + v_m$$

In order to make it easy to write a MATLAB simulation program, Equations (2) and (3) can be further arranged into a matrix form, as follows:

$$E \mathbf{x} = f(\mathbf{x}, i_A)$$

$$v_A = C \mathbf{x}$$

where

$$\mathbf{x} = (x_1 x_2 x_3 x_4)^T = (T \ v_C \ v_m \ i_m)^T$$

$$E = \begin{bmatrix}
1 & 0 & 0 & 0 \\
0 & C & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0
\end{bmatrix}$$

$$f(\mathbf{x}, i_A) = \begin{bmatrix}
0 & 0 & 0 & 0 \\
\frac{v_m + v_m^2 / R_{CNT}}{C_{th}} - \frac{T - T_{amb}}{C_{th} R_{th}} \\
-\frac{v_C}{R} + i_A \\
-\frac{i_m + AT^2 e^{v_m/d - \phi}}{V_{th}} \\
-V_S + R_S i_m + (1 + R_S/R_{CNT})v_m - R_S i_A
\end{bmatrix}$$
The memristor equation is expanded near the operating point.

\[ T = T_0 + \delta T \]
\[ \upsilon_m = V_M + \delta \upsilon_m \]
\[ i_m = I_M + \delta i_m \]  \hspace{1cm} (9)

Here, \( T_0, V_M \) and \( I_M \) are the state, voltage and current values of the DC operating point, respectively.

We can expand the expression of the memristor current near the operating point:

\[ i_m = I_M + \delta i_m = a'_{00}(Q) + a'_{11}(Q)\delta T + a'_{12}(Q)\delta \upsilon_m + h.o.t \]  \hspace{1cm} (10)

where

\[ I_M = a'_{00}(Q) = i_m = AT_0^2 e^{\frac{\beta \sqrt{VM^2 - \delta}}{kT}} \]
\[ a'_{11}(Q) = \frac{\partial i_m}{\partial \upsilon_m} \bigg|_Q = (2T_0 - \frac{\beta \sqrt{VM^2 - \delta}}{k}) Ae^{\frac{-\beta \sqrt{VM^2 - \delta}}{kT_0}} \]
\[ a'_{12}(Q) = \frac{\partial i_m}{\partial \upsilon_m} \bigg|_Q = \frac{\Delta \beta T_0}{2k \sqrt{VM}} e^{\beta \sqrt{VM^2 - \delta}} \]  \hspace{1cm} (11)

\( h.o.t. \) is the higher-order term relative to \( \delta T \) and \( \delta \upsilon_m \). If \( |\delta T| \ll 1 \) and \( |\delta \upsilon_m| \ll 1 \), we can get the following approximate linear relationship:

\[ \delta i_m = a'_{11}(Q)\delta T + a'_{12}(Q)\delta \upsilon_m \]  \hspace{1cm} (12)

Next, we will expand the memristor equation of state with a Taylor series near the operating point \( (V_M, T_0) \):

\[ \frac{d\upsilon_m}{dt} = f(T, \upsilon_m) = f(T_0 + \delta T, V_M + \delta \upsilon_m) = f(T_0, V_M) + b'_{11}(Q)\delta T + b'_{12}(Q)\delta \upsilon_m + h.o.t \]  \hspace{1cm} (13)

where

\[ b'_{11}(Q) = \frac{\partial f(T, \upsilon_m)}{\partial \upsilon_m} \bigg|_Q = -\frac{1}{\upsilon_m C_M} + \frac{V_M (2T_0 - \frac{\beta \sqrt{VM^2 - \delta}}{k}) Ae^{\frac{-\beta \sqrt{VM^2 - \delta}}{kT_0}}}{kT_0} \]
\[ b'_{12}(Q) = \frac{\partial f(T, \upsilon_m)}{\partial \upsilon_m} \bigg|_Q = \frac{1}{\upsilon_m} \left( \frac{\Delta \beta T_0}{2k \sqrt{VM}} e^{\beta \sqrt{VM^2 - \delta}} + AT_0 e^{\beta \sqrt{VM^2 - \delta}} + \frac{2V_M}{C_M kT_0} \right) \]  \hspace{1cm} (14)

Notice that \( f(T_0, V_M) = 0 \), because \( (T_0, V_M) \) is a point on the DC V–I curve. Ignoring the high-order small term, let us linearize the memristor state Equation (13) near the operating point:

\[ \frac{d(\delta T)}{dt} = b'_{11}(Q)\delta T + b'_{12}(Q)\delta \upsilon_m \]  \hspace{1cm} (15)

Taking Laplace transform for Equations (12) and (15), we obtain

\[ \hat{i}_m(s) = a'_{11}(Q)\hat{T}(s) + a'_{12}(Q)\hat{\upsilon}_m(s) \]
\[ s\hat{T}(s) = b'_{11}(Q)\hat{T}(s) + b'_{12}(Q)\hat{\upsilon}_m(s) \]  \hspace{1cm} (16)
The Laplace transforms of $\delta T$, $\delta i_m$ and $\delta v_m$ are $\hat{T}(s)$, $\hat{i}_m(s)$ and $\hat{v}_m(s)$. According to the second formula of (16), we obtain:

$$
\hat{T}(s) = \frac{b'_1(Q)s\hat{i}_m(s)}{s-b'_1(Q)}
$$

According to the first formula of (16) and Equation (17), the admittance function of the memristor can be obtained as follows:

$$
Y(s, Q) \triangleq \frac{\hat{i}_m(s)}{\hat{v}_m(s)} = \frac{a'_{12}(Q)s\hat{i}_m(s)}{s-a'_{12}(Q)} + a'_{12}(Q)
$$

Change Equation (18) into the following form:

$$
Y(s, Q) = \frac{1}{sL_s + R_s} + \frac{1}{R_p}
$$

$Y(s, Q)$ is the admittance of the memristor. The small signal equivalent circuit of the memristor is shown in Figure 5. $L_s$, $R_s$ and $R_p$ are defined as follows:

$$
L_s = \frac{1}{a'_{11}(Q)b_{12}(Q)}, \quad R_s = \frac{(-b'_1(Q))}{a'_{11}(Q)b_{12}(Q)}, \quad R_p = \frac{a'_{12}(Q)}{a'_{11}(Q)}
$$

Figure 5. Small signal equivalent circuit of the memristor.

Considering the DC bias of the cell circuit, according to Equation (2), and that the $R$ and $C$ parameter values do not affect the DC operating point of the system, let $i_A = 0$, $f(x, i_A) = f(x, 0) = 0$, respectively. Then, we use MATLAB to solve the DC operating point $Q$. $(T_0, V_{M_0}, Q) = (3.049042473697802e + 03, 0.0060366246039)$, and substitute the operating point value into Equation (20), we can evaluate $L_s$, $R_s$ and $R_p$ respectively.

The equivalent impedance of port $A$ in the frequency domain is obtained:

$$
Z(j\omega) = Z(s)|_{s=j\omega} = \frac{1}{Y(s, Q)} + \frac{1}{R} + \frac{1}{sC}|_{s=j\omega}
$$

In [18], Professor Chua derived the local active condition of resistive coupled RD-CNNs based on the reaction–diffusion equation. It is said that the cell is in the local active region if the input impedance of the one port cell satisfies at least one of the following conditions:

(a) There is a pole in the right half plane;
(b) There are higher-order poles on the imaginary axis;
(c) There is a pole $s = j\omega_p$ of order one on the imaginary axis and $\lim_{s\to j\omega_p} (s - j\omega_p)Z(s)$ is a negative real number or a complex number with non-zero imaginary part;
(d) There is at least one angular frequency value $\omega$, such that the real part of the impedance $Z(j\omega)$ is less than zero.
Through calculation, the system impedance $Z(s, Q)$ has the following form:

$$Z(s, Q) = \frac{A(s - z_1)(s - z_2)}{(s - p_1)(s - p_2)}$$  \hspace{1cm} (22)$$

where $A$ is the real coefficient. According to Chua’s theory [18], the system described by conditions (a)–(c) is unstable, while the system is a stable local active system when condition (d) is satisfied along with the poles being in the left half plane, that is, the system is located in the edge of chaos. In addition, according to the theory of signals and systems, $Y(s, Q)$ is the transfer function of the system. When the poles of $Y(s, Q)$, corresponding to the zeroes, is located in the right half plane of the complex plane, the system will be unstable, and the system is said to be on the sharp edge of chaos. Specifically, because the numerator of the input impedance is a quadratic polynomial, its zeroes correspond to two cases: the system has two positive zeroes (two zeroes whose real part is greater than zero; they are conjugate zeroes, i.e., $z_1 \neq z_2$, $\text{Re}(z_1) > 0$ and $\text{Re}(z_2) > 0$) or one positive real zero (zero is a positive real number as multiple roots, $z_1 = z_2 > 0$), corresponding to dynamic pattern and static pattern, respectively.

In Figure 6, yellow indicates that the system is in the local passive area and the input impedance does not meet Condition (d); the other areas are in the local active area and the input impedance meets Condition (d). Blue indicates that the system is at the sharp edge of chaos. In this case, the impedance function of the system has two positive zeroes (two zeroes whose real parts are greater than zero; they are conjugate zeroes) or one positive real zero (zero is a positive real number as multiple roots), which correspond to the dark blue and light blue regions, respectively. Other regions in the figure, that is, when green corresponds to other cases of zeroes, indicate that the system is at the edge of chaos. In Figure 6, the edge region of chaos, that is, the light green Region II, contains coupling parameters that may not destabilize the system because the resulting local input impedance of the cell does not have the zero point of the positive real part. On the other hand, the union of the dark blue Region III and the light blue Region IV represents the sharp edge of chaos. In the dark blue Region III, the local input impedance of the cell allows a pair of complex conjugate zeroes with positive real parts, which makes the system unstable and leads to the formation of a dynamic pattern in a steady state. In the light blue Region IV, a zero point of the local input impedance of a single cell is positive and real, which triggers the instability of the system and gradually leads to a static mode. It has been proved by literature [12] that when the cell is in the sleeping mode, the "cell" equation has only a steady-state homogeneous solution; only when the cell is in the sharp edge of chaos can it be successfully “awakened” when it is connected to the CNN; that is to say, the system equation has a non-homogeneous solution, and the light blue region is in so-called “static wake-up”. When a cell is connected to a network, it has a non-homogeneous static solution, which is different from when the cell is isolated; the dark blue region is called a dynamic wake-up, which causes oscillation when the cell is connected to the network, so it has a dynamic oscillation solution, which is different from the static solution when the cell is isolated. Because the capacitance value of static wake-up is too large, it is not practical for an integrated system. Only a dynamic wake-up is considered.
Figure 6. Input impedance characteristic diagram depending on $R$ and $C$ parameters. I—passive region; II—edge of chaos region; III—sharp edge of chaos region (dynamic); IV—sharp edge of chaos region (static).

4. CNN and Simulation

Connect two cells, and the common resistance and capacitance can be equivalent to two identical series connections [12] by the circuit principle, so as to distribute them to each cell, as shown in Figure 7.

$$\tilde{R} = 2R$$
$$\tilde{C} = C/2$$

(23)

Figure 7. The common resistor and capacitor are equivalent to two parts in the series. (a) is the original configuration while (b) is its equivalent circuit.
Select $R = 1 \, \text{M\&Omega;}$, $C = 720 \, \text{p}$, corresponding to $\tilde{R} = 2\, \text{M\&Omega;}$, $\tilde{C} = 360 \, \text{p}$; the two cells are in sleeping mode before coupling, as shown in Figure 8. In Figure 8b, the voltage decreases from 10 V to 0 V, and the cell does not oscillate.

![Figure 8](image)

**Figure 8.** The two cells are uncoupled and in sleeping mode; (a) is the configuration of two uncoupled cells (b) shows there is no oscillation.

After coupling, it is in wake-up mode, as shown in Figure 9. Figure 9b shows that the voltage drops from the initial 10 V to oscillate near 0 V.

![Figure 9](image)

**Figure 9.** Cont.
Figure 9. The cells are in wake-up mode after coupling. (a) is configuration of two coupled cells. In (b), we see there is oscillation in the circuit.

It can be seen from Figures 8 and 9 that when the cell is in the sleeping mode, both cells do not oscillate, and the differential equation of the system has only a trivial solution, that is, a zero solution. When the cell is in wake-up mode, the differential equation of the cell system has oscillatory solutions, and different cells get different oscillatory solutions.

In order to observe the characteristics of a CNN composed of cells, 5 × 5 cells are arrayed, as shown in Figure 10, and the DC excitation of each cell rises to 10 V in 1 µ seconds. The cells in the central position (3,3) are deliberately raised to 10 V in 0.9 µ seconds. The voltage response of 25 cells is observed, as shown in Figure 11.

Figure 10. CNN composed of 5 × 5 cells.
It can be seen from Figure 11 that after a short transient response, each cell reaches steady-state oscillation. According to Figure 11, the network pattern diagram at different times can be made, as shown in Figure 12, in which different colors represent different terminal voltages of the cellular memristor. Figure 12 is just a reproduction of Figure 11 from another view of the spatial distribution of the sampled voltage at a specific time, where, in the vertical axis, “1” represents the highest voltage of the cell, and other values are just the normalized voltage relating to that cell respectively. This is called the pattern of the network. From the figure, it can be seen that the initial conditions can affect the network pattern formation, so that the power source voltage of each cell can be programmed to obtain a specific pattern, so as to complete the information processing.

Figure 11. Terminal voltage response of each memristor.

Figure 12. Cont.
5. Conclusions

In this paper, a CNN based on a VO$_2$ carbon nanotube composite memristor was proposed. The analysis shows that the coupling RC parameters will affect the network pattern formation. According to the local active and edge of chaos theory proposed by Professor Chua, it is pointed out that only when the cell is in the sharp edge of chaos region can the cell be successfully awakened after forming the network, that is, the differential equation of the system has a non-homogeneous solution. If the system equation has a non-homogeneous static solution, it is said that the system is in static mode; if the system equation has an oscillatory solution, it is said that the system is in dynamic mode. When the cell is biased in other regions, the differential equation of the system has only a trivial solution, that is, a zero solution, and the cell is in the sleeping mode. At the same time, the formation of the mode is also affected by the initial conditions. In our experiment, we deliberately made the cells located in the middle of the 5 × 5 CNN network earlier than other cells, so that we could program the cell power supply voltage to get a specific mode and complete the information processing. In summary, the architecture proposed in this paper can be applied to future computing occasions based on complex space–time patterns, especially in the field of computer vision.

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