The method of determining coordinates of an airborne object using ADS-B receivers was improved. The method involves the following sequence of actions: input of initial data, measurement of coordinates of the airborne object by the radar, checking the availability of data about the airborne object obtained from the ADS-B receivers. In the absence of such data, coordinates of the airborne object are determined only from the data of the radar. The airborne object mark was identified according to information from the radar and the ADS-B receivers. Unlike the known methods, the advanced method of determining coordinates of an airborne object by a radar additionally uses information from the ADS-B receivers.

The ADS-B receiver signals were experimentally studied. It was found that the ADS-B receiver has received more than 6,000 messages about airborne objects in a single day. It was established that information about the location of the airborne object contained in ADS-B messages was encoded in CPR format. An algorithm for decrypting the ADS-B messages with a global connection of an airborne object to geographical coordinates was presented. An algorithm for detecting signals of onboard transponders of ADS-B airborne objects was presented. Non-standard ADS-B messages from airborne objects were studied. It was suggested that some short non-standard ADS-B messages were received from small and military airborne objects.

Accuracy of determining coordinates of airborne objects by the radar with additional use of the ADS-B receiver was estimated. Dependence of the root mean square error of determining the airborne object coordinates on a distance to the airborne object presented for various cases. It was established that the accuracy of determining the airborne object coordinates can be raised from 36 % to 67 % depending on the distance to the airborne object.

Keywords: airborne object, method of determination, ADS-B, radar, root-mean-square error, transponder.
The peculiarity of conducting hybrid wars consists in that flights of civil aviation take place in normal mode. As a rule, two-coordinate surveillance radars with mechanical rotation in azimuth are used for conducting radar reconnaissance and airspace control (for example, P-18 type (Ukraine), P-18MA (Ukraine), P-18MU (Ukraine), P-18 Malakhit (Ukraine), etc. Such radars have low accuracy in determining coordinates of airborne objects (AO). As experience has shown, this can lead to the following:

- disguising airborne objects (mainly reconnaissance ones) as objects of civil aviation;
- difficulties in solving the problems of radar reconnaissance and airspace control by radar (radars);
- erroneous destruction of civil airborne objects, etc.

The use of known methods to improve the accuracy of determining coordinates of airborne objects leads to a growth of energy potential of an individual radar and a number of radars in common.

Therefore, it is important to improve the accuracy of determining coordinates of airborne objects in hybrid war conditions.

2. Literature review and problem statement

It is stated in [1] that the aggressor country has a possibility of alternative use of airborne objects violating state borders in conditions of present-day hybrid wars in the absence of open aggression. This is also confirmed in [2] on the example of hostilities in Iraq and Syria. Analysis [1, 2] shows the possibility of disguising the airborne objects violating state borders as civilian scheduled airplanes.

It is noted in [3] that reconnaissance airborne objects will be violators of the state border most of all. This is stated only in [3]. No ways of detecting reconnaissance airborne objects are given in [3]. It is noted in [4] that contrary to international agreements, reconnaissance airborne objects can fly at a fairly short distance from civilian airplanes (about 300 m) (Fig. 1). As can be seen from Fig. 1, both civilian and reconnaissance airplanes (an airborne object violating the state border, e.g., a military airplane, pilotless vehicle, etc.) may be present in one resolution element. All this combined with the development and modernization of airborne objects, means of air attack, the growing intensity of air traffic in the radar inspection area complicates the tasks of radar reconnaissance and airspace control.

Range resolution in radar reconnaissance and airspace control is usually 600 m to 1800 m (e.g., [3]). In this case, radars will not be able to detect and track such reconnaissance airborne objects.

It is known that error in determining an arbitrary coordinate $R\sigma$ of the radar is determined from expression (1) [6]:

$$\sigma_\varepsilon = \frac{\Delta_\varepsilon}{q},$$

where $\Delta_\varepsilon$ is $R$ coordinate resolution; $q$ is the signal-to-noise ratio.

Thus, taking into account expression (1) [6], the known methods of improving the accuracy of determining coordinates of the airborne object are aimed at improving the radar resolution and raising the signal-to-noise ratio.

For example, the methods of spectral estimation are used in [7] to raise resolution. Such methods require additional use of a priori information about the signal parameters being estimated. It is almost impossible to obtain such a priori information in a case of detection of a state border violator. Therefore, the methods [7] are problematic to use. A method of raising the resolution of an unmanned aerial vehicle with optoelectronic surveillance equipment was proposed in [8]. The method [8] can be used to raise optical system resolution. To raise radio system resolution, method [8] is applicable. A method of super-resolution is offered in [9]. The main disadvantage of this study consists in the need to estimate the direct or inverse matrix of input signals. Application of the method of joint search and detection of objects is proposed in [10]. A disadvantage of this study consists in the need for two-stage decision-making procedures and significant time spent for making decisions. This requires a significant amount of calculations, formation of additive and multiplicative noise, reduction of the signal-to-noise ratio, etc.

Petrov-Galerkin’s approach to improving the radar resolution and Hallström’s discerning strategy of solving operator equations are used in the projection method [11]. This method requires additional a priori information (number, position, shape of individual elements of airborne object scattering) as well as knowledge of the type of basic functions to approximate the scatter surface. The disadvantage of this method includes inaccurate or insufficient a priori information, lack of a methodology of forming a priori information to solve practical problems and significant computational costs.

Thus, the main disadvantages of existing methods of improving the radar resolution are as follows:

- the need for a priori information to provide stability and satisfactory computational complexity;
- significant complication of processing algorithms and a sharp rise of computational costs with an increase in the number of discerning signals (number of airborne objects);
- the need for an appreciably small step in the calculation of the objective function when processing the radar signals;
- significant complication of processing algorithms when discerning a mixture of non-orthogonal signals, etc.

To raise the signal-to-noise ratio (reduction of the error in determining coordinates of airborne objects (expression (1)), the study [12] proposes the integration of surveillance radars in multi-radar networks. Methods of coherent signal processing...
in a multi radar net consisting of two surveillance radars were developed in [13]. Integration of radars in a multi-radar network [12, 13] leads to a greater number of surveillance radars and necessitates synchronous operation of surveillance radars in space and time.

To raise the signal-to-noise ratio, the following measures were proposed in [14–16]:
- compaction of disposal of surveillance radars [14];
- use of radars of different ranges [15];
- complication of radar information processing algorithms [16].

The main disadvantages of [14–16] include the need to raise the energy potential of a particular radar, the number of radars, the complexity of methods of processing radar information, etc.

The use of phased arrays in radars as antenna systems is proposed in [17]. This will definitely raise the signal-to-noise ratio. However, restructuring of the antenna system is impossible when the radar is in position and radar reconnaissance and airspace control are conducted.

The use of an active system with external illumination by signals of cellular communication stations is proposed in [18]. A case of detection of airborne objects with the use of a two-position system with additional use of cellular communication signals is considered in [19]. The additional use of cellular communication signals has been shown to raise the signal-to-noise ratio and, consequently, the accuracy of determining airborne object coordinates. The main disadvantages of [18, 19] include the complexity of the synchronization of radars and cellular communication stations and the unresolved issue of optimizing the geometry of multi-position radar systems.

Methods of raising the signal-to-noise ratio through additional use of signals from space navigation systems are proposed in [20]. Synthesized algorithms of processing the navigation signals scattered by airborne objects and a structure of consumer's ground receiving equipment are considered.

A method of raising the signal-to-noise ratio through the introduction of a diverted reception channel in the radar was proposed in [21]. The method involves coordinated signal processing, quadratic detection, weight summation of detector outputs in each processing channel and in each element corresponding to the discrete volume and the corresponding Doppler's discrete frequency. Calculation of parameters of detection zones of surveillance radars with additional use of a channel of diverted reception is given in [22]. The main disadvantage of [21, 22] consists in the need to make design changes in the radar, presence of a powerful penetrating signal in the channel of diverted reception.

To improve the quality of radar reconnaissance of airspace, the use of ADS-B information was proposed in [23]. The information capabilities of ADS-B, types of ADS-B receivers are considered, examples of data received in ASTERIX protocol (category 21) and in Advanced Virtual RISC (AVR) codes are given. This study states that the use of ADS-B data can provide additional information on airborne objects. However, it just states the possibility of obtaining additional ADS-B information, does not calculate errors in determining coordinates of airborne objects, etc.

Therefore, the use of information from ADS-B receivers as additional information during radar reconnaissance and airspace control can significantly raise the accuracy of determining coordinates of the radar airborne objects. So, the development of a method of determining coordinates of the radar's airborne objects with the additional use of ADS-B receivers is an urgent task.

3. The aim and objectives of the study

The study objective implies the improvement of a method for determining the position of airborne objects with additional use of ADS-B receivers. This will improve the accuracy of determining coordinates of airborne objects violating the state borders.

To achieve this objective, it was necessary to solve the following tasks:
- to determine main stages of the method of determining coordinates of airborne objects with additional use of ADS-B receivers;
- to study signals of ADS-B receivers;
- to estimate the accuracy of determining coordinates of airborne objects of the radar with additional use of ADS-B receivers.

4. The study materials and methods

The underwritten methods were used in the study.

When determining the main stages of the method of determining coordinates of radar airborne objects with additional use of ADS-B receivers, the following methods were used: methods of radar theory, methods of probability theory and mathematical statistics, methods of system analysis, methods of multiposition radiolocation, methods of differential calculus, methods of digital signal processing and mathematical apparatus of matrix theory.

When studying the ADS-B receiver signals, methods of radar theory, methods of probability theory and mathematical statistics, methods of mathematical modeling, methods of differential calculus, methods of digital signal processing, mathematical apparatus of matrix theory, methods of the statistical theory of detection and measurement of radar signals were used.

When estimating the accuracy of determining coordinates of radar airborne objects with additional use of ADS-B receivers, methods of radar theory, methods of probability theory and mathematical statistics, methods of mathematical modeling, methods of multi-position radiolocation, methods of digital signal processing, and mathematical apparatus of matrix theory were used.

Analytical and empirical methods of comparative study were used in the estimation of the proposed solutions.

The following limitations and assumptions were elaborated during the study:
- two-coordinate surveillance radars with mechanical rotation of P-18 type (Ukraine), P-18MA type (Ukraine), P-18MU type (Ukraine), P-18 Malakhit (Ukraine) were considered;
- radio receivers were of digital design;
- it was considered that there are no radio interferences;
- unimpeded signal reception from onboard ADS-B transponder was provided;
- RLT-SDR receiver was used as an ADS-B receiver: DVB-T+FM+DAB 820T2 & SDR (antenna included).
5. The results obtained in studying the development of a method for determining coordinates of airborne objects

5.1. Main stages of improving the method of determining coordinates of airborne objects

To define the main stages of the method of determining coordinates of airborne objects with additional use of ADS-B receivers, a case of positioning the ADS-B receiver at the radar position was considered (Fig. 2).

The radar measures angular coordinates \((D, \beta)\) where \(D\) is the distance to the airborne object, \(\beta\) is azimuth to the airborne object. In so doing, it is possible to find in the radar inspection area the airborne objects that are not equipped (airborne object 1 (AO1) and equipped (airborne object 2 (AO2)) with ADS-B transponders. In the case of equipping the AO2 with an ADS-B transponder, the ADS-B receiver will measure geodetic coordinates of the AO2 \((B, L)\) where \(B\) is latitude, \(L\) is longitude.

The main stages of the algorithm of improving the method of determining the airborne object coordinates using data from ADS-B receivers are shown in Fig. 3.

In this case, the airborne object will be understood as AO2 equipped with an ADS-B transponder (Fig. 2).

The method of determining the AO coordinates using ADS-B receivers involves the following basic steps:

1. Input of source data: BC of the radar (resolution by the range and angular coordinates, accuracy of determining the AO coordinates, etc.), BC of ADS-B receivers.
2. Measuring the AO coordinates.
3. Checking availability of AO data from ADS-B receivers.
4. In the absence of AO data from ADS-B receivers, they are determined using the radar data solely.
5. When data from ADS-B receivers are available, the AO coordinates are measured using the data from ADS-B receivers.
6. Identification of the mark from the airborne object according to the radar and ADS-B data (speed, course, coordinates, etc.). The airborne object height is taken into account only when using three-coordinate radars.

7. Determining the AO coordinates using data from ADS-B receivers (AO type, registration number, affiliation, call sign, coordinates, etc.).

Thus, a method of determining coordinates of the radar airborne object has been developed in which (unlike the known methods) information of ADS-B receivers is additionally used.

5.2. Experimental studies of the ADS-B receiver signals

5.2.1. Initial data on conducting experimental studies

Experimental studies of the ADS-B receiver signals were conducted based on Admiral Makarov National University of Shipbuilding (Mykolaiv, Ukraine). The RLT-SDR receiver was used: DVB-T+FM+DAB 820T2 & SDR (antenna included) (Fig. 4).

The receiver specification:
- frequency range: 24–1750 MHz;
- modulation type: FM, AM;
- bandwidth: 0.25–3 MHz;
- sensitivity: 220 mV;
- input resistance in reception: 50 Ohms;
- range filters: external only;
- bit-to-digital converter bit size: 8 bits;
– dynamic range: 50 dB;
– delay of signal detection: 340 ms;
– interface: USB 2.0.

5.2.2. Experimental data obtained in one observation day

The ADS-B receiver (China) received more than 6,000 messages on airborne objects in one day. For example, airborne object 50816F (a civil Embraer airplane, Brazil) was observed for about 5 minutes and for about 10 minutes. Fig. 5, 6 show information from the Flightradar24 website (the site server in Sweden) regarding the airborne object 50816F (civil airplane Embraer). It was established that this airplane was flying on Kyiv-Kherson and Kherson-Kyiv routes.

More than 800 messages were received from the airborne object 4B906C (French Airbus A320 civil airplane). It was established that this civilian airplane was flying from Kharkiv to Istanbul (Fig. 7).

The solid blue line in Fig. 5–7 marks flights of airborne objects in the route map. ADS-B messages from airborne object transponders were decrypted.

5.2.3. Decrypt the ADS-B messages

Information on airborne object location in the ADS-B messages is encoded in Compact Position Reporting (CPR) format aimed to encode more characters in geographic coordinates using fewer bits. The main idea of CPR consists in dividing the earth's surface into zones and transmitting the zone number instead of geographical coordinates. The number of latitude zones from the equator to the pole is \( NZ=15 \) for Mode-S. The number of longitude zones \( NL \) depends on latitude \( \text{lat} \) and is given by expression (2).

The number of longitude zones varies from 1 for polar latitudes to 59 for equatorial latitudes.
Information and controlling system

Two messages, multiple and non-multiple, are generated to initially link the airborne object to geographical coordinates. Knowing the previous location of the airborne object, information about geographical coordinates can be extracted from each message. When the airborne object is globally connected to geographical coordinates, the decryption algorithm is as follows:

1. The obtained data $\text{Lat}_{\text{cprEven}}, \text{Lat}_{\text{cprOdd}}, \text{Lon}_{\text{cprEven}}, \text{Lon}_{\text{cprOdd}}$ are transformed into the format with a floating point numbers.

2. The latitude index is calculated from expression (3):

   $$j = \text{floor}(59\text{Lat}_{\text{cprEven}} - 60\text{Lat}_{\text{cprOdd}} + 0.5).$$  

3. Relative latitude is calculated from expressions (4), (5):

   $$\text{Lat}_{\text{Even}} = \text{dLat}_{\text{Even}} \times (\text{mod}(j, 60) + \text{Lat}_{\text{cprEven}});$$  

   $$\text{Lat}_{\text{Odd}} = \text{dLat}_{\text{Odd}} \times (\text{mod}(j, 59) + \text{Lat}_{\text{cprOdd}}).$$

   where

   $$\begin{align*}
   \text{dLat}_{\text{Even}} &= (360/(4NZ)) - (360/60); \\
   \text{dLat}_{\text{Odd}} &= (360/(4NZ - 1)) - (360/59)
   \end{align*}$$

4. To ensure membership of the range $[-90^\circ, 90^\circ]$, the calculated values are corrected, if necessary, according to expressions (6), (7):

   $$\text{Lat}_{\text{Even}} = \text{Lat}_{\text{Even}} - 360 \text{ if } (\text{Lat}_{\text{Even}} \geq 270);$$  

   $$\text{Lat}_{\text{Odd}} = \text{Lat}_{\text{Odd}} - 360 \text{ if } (\text{Lat}_{\text{Odd}} \geq 270).$$

5. Later messages are used as the final value of latitude (expression (8)):

   $$\text{Lat} = \begin{cases} 
   \text{Lat}_{\text{Even}}, \text{ if } (T_{\text{Even}} \equiv T_{\text{Odd}}); \\
   \text{Lat}_{\text{Odd}}, \text{ otherwise.}
   \end{cases}$$

6. Longitude zone numbers are determined for both latitude values $\text{NL} (\text{Lat}_{\text{Even}})$ and $\text{NL} (\text{Lat}_{\text{Odd}})$ using expression (2). If they are different, it is impossible to calculate global longitude and it is necessary to wait for the next pair of messages.

7. In the case of the coincidence of numbers of longitude zones for both values of latitude, it is necessary to calculate global longitude. If the time of multiple messages is greater than the alignt time, the following calculations must be performed (expressions (9) to (12)):

   $$\begin{align*}
   ni &= \max(\text{NL}(\text{Lat}_{\text{Even}}), 1); \\
   \text{dLon} &= \text{360}/ni;
   \end{align*}$$

8. The longitude values exceeding $180^\circ$ are adjusted using expression (17):

   $$\text{Lon} = \text{Lon} - 360, \text{ if } (\text{Lon} \geq 180).$$

Information on the airborne object altitude above sea level comes in the same message as the geographical coordinates. Altitude calculations using it do not depend on the message parity and are always given in feet. The incoming data contain information on the accuracy of measuring the airborne object altitude. This information is given by the so-called Q-bit. If its value is “0”, then altitude discreteness 100 feet. If otherwise, then expressions (13)–(16) are used:

$$\begin{align*}
\text{Lon} &= \text{Lon}_{\text{Even}} \times (\text{mod}(m, ni) + \text{Lon}_{\text{cprEven}}); \\
\text{Lon} &= \text{Lon}_{\text{Odd}} \times (\text{mod}(m, ni) + \text{Lon}_{\text{cprOdd}}).
\end{align*}$$

8. The longitude values exceeding $180^\circ$ are adjusted using expression (17):

   $$\text{Lon} = \text{Lon} - 360, \text{ if } (\text{Lon} \geq 180).$$

According to (18) and number of the bits bearing the altitude information (11 bits), the range of altitudes that can be encoded is 1000 to 2$^{11-1}$=1000–50,175 feet or 305 to 15,293 meters for Q-bit=1.

Local connection of an airborne object to geographical coordinates presupposes knowledge of the reference point in the vicinity of which the airborne object is located. This can be data obtained from previous messages or data on the location of the receiving antenna. A message with any parity can be used. With local connection, latitude is calculated using expressions (19) to (21):

$$\begin{align*}
\text{Lat} &= \text{Lat} (j + \text{Lat}_{\text{ref}}); \\
\text{dLat} &= \begin{cases} 
360/60, \text{ if number of message is Even}; \\
360/59, \text{ if number of message is Odd};
\end{cases}
\end{align*}$$

$$\begin{align*}
\text{Lon} &= \text{Lon}_{\text{cprEven}} \times [\text{NL}(\text{Lat}_{\text{Even}}) - 1] - \text{Lon}_{\text{cprOdd}} \times \text{NL}(\text{Lat}_{\text{Odd}}) + 0.5; \\
\text{Lon} &= \text{Lon}_{\text{cprEven}} \times [\text{NL}(\text{Lat}_{\text{Odd}}) - 1] - \text{Lon}_{\text{cprOdd}} \times \text{NL}(\text{Lat}_{\text{Odd}}) + 0.5.
\end{align*}$$

$$\begin{align*}
\text{Lon} &= \text{Lon} \times (\text{mod}(m, ni) + \text{Lon}_{\text{cprEven}}); \\
\text{Lon} &= \text{Lon} \times (\text{mod}(m, ni) + \text{Lon}_{\text{cprOdd}}).
\end{align*}$$

$$\begin{align*}
\text{Lon} &= \text{Lon} - 360, \text{ if } (\text{Lon} \geq 180).$$
\end{align*}$$
The received sync pulses are quite distorted (usually, the correlation coefficient does not exceed 0.7). In the algorithm under consideration, if the maximum coefficient among the calculated correlation coefficients exceeds the set threshold $\text{corrThreshold}=0.68$, then this sample is taken as the beginning of the clock pulse and bits are allocated on the interval of the long message. “1” is formed if the sum of the first 6 samples exceeds the sum of the next 6 samples, otherwise “0” is formed. Regardless of the length of the transmitted message, it is decoded as a long one. The message is translated into hexadecimal form and the CRC code is checked. If the CRC matches, receiving a long message is guaranteed. If not, the received characters are truncated to 56 bits (14 digits) and the hypothesis of receiving a short message by a new calculation of the CRC code is checked. The $\text{crc24f}()$ function which implements a 24-bit CRC based on the universal comm.$\text{CRCDetector}()$ function is used to check the CRC code. It should be noted that regardless of the length of the message, the probability of a random match of the 24-bit CRC code is equal to $\frac{1}{2^{24}} \approx 6 \times 10^{-8}$, which virtually guarantees error-free decoding of all messages.

5.2.4. Detecting signals of onboard airborne transponders ADS-B

Information from the receiver output is immediately passed through a square-law detector (complex readings are replaced by amplitudes). Amplitudes at the output of the square-law detector are interpolated to raise quantization frequency from 2.4 MHz to 12 MHz. Additional readings are built based on the reconstruction or anti-imaging FIR filter.

Detection of on-board signals begins with the selection of samples that exceed average background by 14 dB, i.e. average level of amplitude throughout the frame is calculated and samples with amplitude not less than 5 times the average value are selected. For such samples, the zone of the possible presence of a signal with an indentation by samplesBeforeSyncPulse=60 samples before the selected sample and by samplesAfterMessage=120 samples after the expected long message is formed. The number of samples in the extended zone is 1524 (sync pulse length of 96 samples in the short message and 1248 samples in the long message). A standard sample correlation coefficient with a known sinc pulse is calculated for the first 85 samples of this zone. A sync pulse of a standard ADS-B message is shown in Fig. 8.

$$
\text{Lon} = \text{dLon} (m = \text{Lon}_{ref}):
\begin{align*}
\text{dLon} &= \begin{cases} 
360 \text{NL}(\text{Lat}), & \text{if NL}(\text{Lat}) > 0; \\
360, & \text{if NL}(\text{Lat}) = 0;
\end{cases} \\
m &= \text{floor} \left( \frac{\text{Lon}_{ref}}{\text{dLon}} \right) + \\
+ \text{floor} \left( \frac{\text{mod}(\text{Lon}_{ref}, \text{dLon}) - \text{Lon}_{ref} + 0.5}{\text{dLon}} \right),
\end{align*}
$$

where $\text{Lon}_{ref}$ is the longitude of the reference point.

5.2.5. Study of non-standard ADS-B messages from airborne objects

Non-standard ADS-B signals were detected during experimental studies. The CRC code matches such messages. However, such messages are not detected with the enabled detection of a given sync pulse or other systems for working with ADS-B Mode-S signals. Study of the Frame20210224.bin file with amplitude recordings during one day was performed by the ADS-B signal detection program with sync pulse detection on and off. It was established that with the sync pulse detection turned off, some standard signals are detected which are determined with the sync pulse detection on. Their AirplanesID number was determined without errors but the rest of the message was received incorrectly, with substantial errors. In addition to the standard signals when detection of a given sync pulse is turned off, there was a significant number of non-standard short messages (or fragments of messages) starting with the letters VA and BE. For example, there were 13 detected standard signals for 13 detected standard signals. In total, the Frame20210224.bin file contained 239 short non-standard messages. The probable sync pulse of non-standard ADS-B messages is shown in Fig. 9.

According to the analysis results, a substantial part of board numbers of airborne objects received in short non-standard ADS-B messages is in the Flightradar24 net. However, there is almost no information about types of airborne objects or their flights, except for some boards. For example, there is no information on the following airborne objects with flight numbers A106CD, 975327, 975328, 975A60, 975333, 972D15, 9720C2, 977082, 97708D, 9720C2 in the Flightradar24 network. The specialized aviation online register Planespotters.net does not contain any information about airborne objects with determined board numbers.
Attention was drawn to some board numbers of airborne objects from which non-standard ADS-B messages were received (e.g. A106CD). They were compared with the ICAO code format of the airborne object. Based on this information, it can be assumed that the first part of the board number of airborne objects may be an ICAO code. For example, A106CD would correspond to ICAO code A106. This assumption is relevant for small airplanes. However, in this case, 256 values remain for the individual number in the series which is quite small. A complete list of ICAO codes is not freely available, so it is impossible to confirm or deny this assumption.

Thus, it can be assumed that some short non-standard ADS-B messages are received from small airplanes. The lack of any data on the rest of the detected messages suggests that military airborne objects are their source.

5.3 Estimation of accuracy of determining coordinates of airborne objects by a radar with additional use of the ADS-B receiver

Experimental studies of the method of determining coordinates of airborne objects with the additional use of the ADS-B receiver were conducted. P-18MA radars (Ukraine) were used. Let us make a comparative estimation of the accuracy of determining coordinates of airborne objects using various methods. Theoretical calculations were performed to raise the accuracy of determining coordinates of airborne objects. Root mean square (RMS) error of determining coordinates of the airborne object was used as an accuracy indicator (e.g., [24, 25]). The resulting RMS error of determining coordinates of the radar airborne object with additional use of the ADS-B receiver is determined by expression (25):

\[
\sigma_\Sigma = \sqrt{\sigma_{\text{Radar}}^2 + \sigma_{\text{ADS-B}}^2}
\]

where \(\sigma_\Sigma\) is the resulting RMS error of determining coordinates of the radar airborne object with additional use of the ADS-B receiver;

\(\sigma_{\text{Radar}}\) is RMS error of determining coordinates of the airborne object using the radar solely;

\(\sigma_{\text{ADS-B}}\) is the RMS error of determining coordinates of the airborne object using the ADS-B receiver.

Fig. 13 shows the dependence of RMS error of determining coordinates of the airborne object on the distance to the airborne object for various cases. For example, line 1 shows the dependence of \(\sigma_{\text{Radar}}\) on the distance to the airborne object using the radar data only. Line 2 shows the dependence...
of $\sigma_{ADS-B}$ on the distance to the airborne object using ADS-B receivers. Line 3 shows the dependence of $\sigma_R$ on the distance to the airborne object using the radar data with additional use of the ADS-B receiver.

![Graph showing the dependence of the root mean square error of determining coordinates on distance to the airborne object.](image)

Fig. 13. Dependence of the root mean square error of determining coordinates of an airborne object on the distance to the airborne object for various cases

It can be concluded from the analysis of Fig. 13 that the accuracy of determining coordinates of the airborne object can be raised from 36% to 67% depending on the distance to it.

6. Discussion of the results obtained in studying the development of a method of determining the airborne object coordinates

The main stages of improvement of the method of determining coordinates of the radar airborne object with additional use of ADS-B receivers are given in Fig. 3. This method involves the following sequence of steps: input of initial data, measurement of coordinates of the airborne object using the radar, checking the availability of data about the airborne object obtained from the ADS-B receivers. In the absence of such data, coordinates of the airborne object are determined only by using the radar data. The mark from the airborne object is identified according to the radar and the ADS-B data. Thus, the method of determining coordinates of the radar airborne object has been improved. Information of ADS-B receivers is additionally used in this method, unlike the known methods.

Experimental studies of the ADS-B receiver signals were performed. The RLT-SDR receiver was used: DVB-T + FM + DAB 820T2 & SDR (antenna included) (Fig. 4). It was found that more than 6,000 messages on airborne objects were received in one day of the ADS-B receiver operation. It was also found that more than 800 messages were received from 4B906C airborne object. It was established that it was a civilian airplane flying from Kharkiv to Istanbul (Fig. 7). The decryption of ADS-B messages is given. It was established that information about the location of the airborne object in ADS-B messages is encoded in CPR format. The main CPR idea consists in dividing the earth's surface into zones and transmitting the zone number instead of its geographical coordinates (2). An algorithm of decryption of the ADS-B messages with a global connection of airborne objects to geographical coordinates (3) was presented. An algorithm for detecting signals of onboard ADS-B transponders of airborne objects was given. A sync pulse of the standard ADS-B message was presented (Fig. 8). Non-standard ADS-B messages from airborne objects were studied. The probable sync pulse of non-standard ADS-B messages was presented (Fig. 9).

It has been suggested that some short non-standard ADS-B messages are received from small airplanes. Also, the lack of any data on the rest of the detected messages suggests that military airborne objects are their source.

Accuracy of determining coordinates of airborne objects by the radar with additional use of the ADS-B receiver was estimated. The P-18MA radar (Ukraine) was used. Value of RMS error was used as an indicator of accuracy (expression (25)). Dependence of the RMS error of determining the airborne object coordinates on the distance to the airborne object was shown for various cases (Fig. 13). It was established that the accuracy of determining the airborne object coordinates can be raised from 36 % to 67 % depending on the distance to the airborne object.

The study has the following limitations and assumptions:
- surveillance two-coordinate radars with mechanical rotation of P-18 type (Ukraine), P-18MA (Ukraine), P-18MU (Ukraine), P-18 Malakhit (Ukraine) were considered;
- radar radio receivers are of digital design;
- it is assumed that there are no interferences;
- unimpeded signal reception from the onboard transponder ADS-B is provided;
- RLT-SDR receiver is used as the ADS-B receiver: DVB-T+FM+DAB 820T2 & SDR (antenna included).

It is expedient that further studies should be focused on the development of methods for determining coordinates of airborne objects that are not equipped with ADS-B transponders and radars.

7. Conclusions

1. The advanced method of determining coordinates of airborne objects using the ADS-B receivers involves the following sequence of actions: input of initial data, measurement of coordinates of the airborne object by the radar, checking the availability of data received from ADS-B receivers about the airborne object. In absence of such data, coordinates of the airborne objects are determined only by using data of the radar. The airborne object mark is identified according to the radar and ADS-B data. Unlike the known methods, the developed method of determining coordinates of the airborne object additionally uses information of the ADS-B receivers.

2. Experimental studies of the ADS-B receiver signals were performed. It has been established that more than 6,000 messages on airborne objects were received in one day of the ADS-B receiver operation. It was established
that information about the location of airborne objects in ADS-B messages is encoded in CPR format. An algorithm of decoding the ADS-B messages when the global connection of an airborne object to geographical coordinates was provided. An algorithm for detecting signals of onboard ADS-B transponders of airborne objects was presented. A study has been conducted on non-standard ADS-B messages from airborne objects. It has been suggested that some short non-standard ADS-B messages are received from small airplanes. The lack of any data on the rest of the detected messages suggests that military air objects are their source.

3. Accuracy of determining coordinates of airborne objects by the radar with additional use of the ADS-B receiver was estimated. Dependence of RMS errors of determining coordinates of airborne objects on the distance to the airborne object was presented for various cases. It was established that the accuracy of determining coordinates of the airborne object can be raised from 36 % to 67 % depending on the distance to the airborne object.

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