A Numerical Approach to Design the Kretschmann Configuration Based Refractive Index Graphene-MoS2 Hybrid Layers With TiO2-SiO2 Nano for Formalin Detection

Md. Biplob HOSSAIN1*, Tamanna TASNIM2, Lway F. ABDULRAZAK3, Md. Masud RANA2, and Md. Rabiul ISLAM4

1Department of Electrical and Electronic Engineering, Jashore University of Science and Technology, Jashore-7408, Bangladesh
2Department of Electrical and Electronic Engineering, Rajshahi University of Engineering & Technology, Rajshahi-6402, Bangladesh
3Department of Computer Science, Cihan University Slemani, Sulaimaniya-46001, Iraq
4School of Electrical Computer and Telecommunications Engineering, Faculty of Engineering and Information Sciences, University of Wollongong, NSW 2522, Australia

*Corresponding author: Md. Biplob HOSSAIN E-mail: biplobh.eee10@gmail.com

Abstract: In this paper, a Kretschmann configuration based surface plasmon resonance (SPR) sensor is numerically designed using graphene-MoS2 hybrid structure TiO2-SiO2 nano particles for formalin detection. In this design, the observations of SPR angle versus minimum reflectance and SPR frequency (F_{SPR}) versus maximum transmittance (T_{max}) are considered. The chitosan is used as probe legend to perform reaction with the formalin (40% formaldehyde) which acts as target legend. In this paper, both graphene and MoS2 are used as biomolecular acknowledgment element (BAE) and TiO2 as well as SiO2 bilayers is used to improve the sensitivity of the sensor. The numerical results show that the variation of F_{SPR} and SPR angles for inappropriate sensing of formalin is quite insignificant which confirms the absence of formalin. On the other hand, these variations for appropriate sensing are considerably significant that confirm the presence of formalin. At the end of this article, the variation of sensitivity of the proposed biosensor is measured in corresponding to the increment of a refractive index with a refractive index step 0.01 refractive index unit (RIU). In inclusion of TiO2-SiO2 bilayers with graphene-MoS2, a maximum sensitivity of 85.375% is numerically calculated.

Keywords: Surface plasmon resonance formalin detection; graphene; refractive index; sensitivity

1. Introduction

Formalin is an ecologically extensively chemical compound that causes cancer to humans [1]. Exposure to formalin will possibly cause antagonistic health effects. It is the greatest practical contact allergen in metal working fluids [1]; toxic incident can cause ecological hypersensitivity and
chronic worsening disease [1]. Formalin is a poisonous element which contains 40% formaldehyde soluble in water [2]. Formaldehyde travels the blood throughout the body and rejoins with proteins, abolishing their biological function. Also, it can react with an amine functional group of the amino acid lysine in a protein, called rhodopsin. Formaldehyde also reacts with amino groups in other proteins, including many enzymes, and the loss of the function of these biological catalysts causes death [1]. Recent news and research have explored the frequent use of formaldehyde in food preservation, which is very popular, particularly in Asian region [2]. Therefore, the accurate detection of formalin is a serious national issue, which is a biochemical process. Its mechanism of action for fitting deceits in its aptitude to form cross-links between soluble and structural proteins. The resulting structure holds its cellular constituents in them in vivo associations to each other, giving it a degree of mechanical strength, which permits it to survive subsequent processing [3].

Many conventional procedures are available for the detection of formaldehyde, enzyme detection, food safety, and environmental monitoring [4–7]. These procedures are Deniges and Eegriwes methods [4], gas chromatography-mass spectrometry (GC-MS) [5], high performance liquid chromatography (HPLC) [6], fluorimetry [7], Nash test [7], gravimetric methods [6], and other chemical based procedures. Unfortunately, these methods, reagents, and reaction products are often harmful to human health. The conventional methods require similarly hazardous reagents and suffer from a number of interferences, resulting in false positions. Additionally, conventional methods are impracticable for real-time measurements [1]. To overcome the drawbacks of the conventional procedures and meet the requirement of concerned issue, the biosensor technology can play a significant role in the solution.

In recent years, refractive index based surface plasmon resonance (SPR) bio-sensing has been widely researched because this sensor technology has a great potential for detection and analysis of chemical and biochemical substances in many important areas including medicine, biotechnology, monitoring of drug, food quality, environment safety, formalin detection, medical diagnosis, enzyme detection, and doxyribonucleic acid (DNA-DNA) hybridization [8–19].

The collective oscillation of metallic electrons in the presence of time varying electromagnetic field at the meta-dielectric interface is defined as SPR [19–25]. Plasmons are stand-alone solutions of Maxwell’s equations consisting in collective excitations of charge, which move coherently with a common frequency and wave-vector [19]. While bulk plasmons are related to bulk systems, surface plasmons waves (SPW) that propagate along the metal-dielectric interface [19–22]. When the phase matching condition between incident wave and surface plasmons wave is satisfied, the externally shined light gets coupled with the surface plasmon modes of the metal-dielectric interface giving birth to the propagating oscillation in the longitudinal direction and evanescently decaying in transverse directions [19]. The condition of phase matching is found to be met only with the transverse magnetic (TM) polarization mode of the incident light [26]. Since the direct light does not carry enough momentum to excite surface plasmons at the desired interface, Kretschmann configurations have been proposed to provide light the extra momentum [22–25]. In these configurations, the light gets its extra momentum from the high refractive index of the dielectric material of prism [20]. The SPR technique is successfully applied to detect the presence of formalin in sample biomolecules.

Numeral SPR biosensors have been industrially advanced, and among them the compact surface plasmon (CSPR) sensor [27], the optical sensing surface plasmon resonance (OSSPR) sensor [28], the localized surface plasmon resonance (LSPR) sensor
[29, 30], and the long-range surface plasmon resonance (LRSPR) sensor [31, 32] have the benefits of compactness, lightness in weight, high sensitivity, the case of multiplexing and remote sensing, and so on. Fundamentally, there is no major difference in operating principle among the above-mentioned sensors. LRSPRs are surface electromagnetic waves that can be created on thin metallic films entrenched between two identical refractive index dielectrics [31, 32], on the other hand, LSPR can be used on the metal-dielectric interface with different refractive indexes to generate SPW [29, 30]. In LSPR, the variation of the concentration of biomolecules owing to chemical reaction will make a local change of surrounding refractive index near the sensor surface [29]. This change of refractive index results in a change of propagation constant of the SPW and thus the SPR angle and SPR frequency ($F_{SPR}$) change [10]. The principle of OSSPRs is the same with LSPRs except that it is fabricated in optical fiber cables [12, 17, 28]. Compared with these SPR biosensors, the LRSPRs have longer surface propagation lengths, higher surface electric field strengths, and narrower angular resonance curves [32]. The LSPRs offer better sensitivity, robustness, and facile detection [29]. OSSPRs accept the benefits of remote sensing applications [33].

One of the key ingredients of any sensing device is the binding/adsorbing material with a large surface area [9, 14, 21], and the graphene and MoS2 have attracted a considerable amount of attention interestingly because of their large band gap [14], high optical absorption efficiency [34, 35], and large work function [12]. Titanium dioxide (TiO2) is one of the most widely used semiconductors in photocatalysis and solar energy conversion [22]. As an SPR sensitive material, it has distinguished advantages such as low cost, high stability, high permittivity, and environmental friendliness [16, 18, 36, 37]. The silicon dioxide (SiO2) layer also increases the sensitivity of the probe [16, 18, 38, 39]. The porous TiO2 & SiO2 film gives us a huge surface area to maximize the amount of incident light that can be absorbed. For this reason, TiO2-SiO2 nano particles show tremendous plasmonic effect near TiO2-SiO2 interface facilitating effective light trapping. This effective light trapping generates more surface plasmons (SPs) which will eventually enhance the SPR angle and frequency. This rise of SPR angle and frequency will increase the sensor sensitivity [16, 38].

In the current study, numerical Kretschmann configuration based refractive index sensor utilizing graphene-MoS2 hybrid layers with TiO2-SiO2 nano particles is designed and investigated, which can explore a new window for the detection of formalin. A composite graphene-MoS2-Au-TiO2-SiO2 layer is used for faster immobilization by monitoring the change of SPR angle-minimum reflectance attributor and SPR frequency-maximum transmittance attributor. Finally, the influence of adding TiO2-SiO2 with graphene-MoS2 is investigated, which results in a higher sensor sensitivity of 85.375% compared with the conventional structure reported. At the end of this article, a study of the variation of sensitivity of the proposed biosensor is measured in corresponding to the increment of a refractive index with a refractive index step 0.01 refractive index unit (RIU).

### 2. Methodology and theoretical design strategy

The proposed SPR biosensor is composed of seven layers, of which the configuration is shown in Fig. 1. The incident light in the transverse magnetic (TM) polarization state is the most important condition for excitation of SPs [22]. For an inciting TM polarized light, a polarizer is used in the way of incident. For the angular interrogation method, the Kretschmann arrangement based sensor, this paper considers the Fresnel optical system to design the proposed sensor which was discussed in detail in [9–16]. To give extra momentum to the incident
light, high wave vector photonic crystals need to be used [40]. So to fulfil this condition, we specify high refractive indexed prism, such as SF11 glass prism, as a base layer having a high refractive index \( n_p \), which is shown in Table 1. In this paper, gold is used to maintain good resistance from oxidation and corrosion, better chemical stability, and superior optical performances [9, 22]. A resonant excitation of photon-electron coupling takes place when the wave vector of the incident light remains confined at the interface and decays exponentially in the transverse directions [14, 41].

Table 1 Sensor layers’ description with the optimized material’s geometries.

| Position | Layer materials | Refractive index (n) (RIU) | Optimized thickness (d) (nm) | References |
|----------|-----------------|--------------------------|-------------------------------|------------|
| 1st      | SF11 glass prism | \( n_1=1.7786 \)           | ---                           | [12, 18]   |
| 2nd      | Porous TiO2      | \( n_2=2.5837 \)           | \( d_2=37 \)                  | [16, 18]   |
| 3rd      | Porous SiO2      | \( n_3=1.4570 \)           | \( d_3=20 \)                  | [16, 18]   |
| 4th      | Gold (Au)        | \( n_4=0.1838 +i3.4313 \)  | \( d_4=20 \)                  | [9, 11, 16, 18] |
| 5th      | MoS2             | \( n_5=5.9+i0.8 \)         | \( d_5=0.65 \)                | [18, 39]   |
| 6th      | Graphene         | \( n_6=3.0 +i1.1487 \)     | \( d_6=0.34 \)                | [42–44]    |
| 7th      | PBS solution     | \( n_7=1.34 \)             | ---                           | [45, 46]   |

The evanescent tail of SPR is very sensitive to changes in a complex refractive index of a metal layer, surrounding dielectric medium, and their geometrical sizes [14, 22], which results in high sensor sensitivity [22]. For accelerating sensitive changes of tail in SPR evanescent wave to obtain a high sensor sensitivity, we select graphene and MoS2 which have high complex refractive index as well as high carrier mobility, high optical transparency, exceptional mechanical flexibility, mechanical strength, low resistivity, tunable conductivity, and extreme mode confinement [47–50]. And the final layer is phosphate buffer saline (PBS) solution as bare sensing dielectric medium, which affords better adsorption of biomolecules [45, 46]. A complete theoretical configuration of the proposed sensor with the optimized material’s geometries has been summarized in Table 1. After confirming the setup, a TM polarized He-Ne light with a wavelength of 633 nm is used, which passes through the prism and some portion is reflected at the composite layer interface.

At the time of ongoing light energy to composite layer interface, an evanescent momentary wave is produced which is known as SPW mentioned in the section that propagates with a dissimilar propagation constant from light wave. The propagation constant of SPW can be adjusted in such a way that it equals to the propagation constant of optical wave in order to obtain surface resonance. The point at which the optical wave propagation constant equals to the SPW propagation constant is called SPR point [12]. As expressed in (1), the SPR angle is a refractive index dependent parameter of the sensing medium. At the SPR point, the frequency at which SPW propagates is called surface plasmon resonance frequency \( F_{SPR} \) [10] and the angle of incidence is called SPR angle [10–12] that can be expressed by (1) [12, 16, 18]:

\[
\theta_{SPR} = \sin^{-1} \left( \frac{n_{eff} n_{sens}}{n_{prism} \sqrt{n_{eff}^2 + n_{sens}^2}} \right)
\]

where \( n_{prism} \) and \( n_{sens} \) are the refractive indexes of SF11 glass prism \( (n=1.7786) \) and sensing dielectric medium \( (n=1.34 \text{ for PBS in bare sensor}) \), respectively; \( n_{eff} \) refers to the equivalent refractive index of Graphene-MoS2-Au metallic with...
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TiO$_2$-SiO$_2$ nano composite layers which are defined in [12, 16, 18]. When formalin is fleeting into chitosan on the sensor medium, the refractive index of sensing medium is modified owing to performing chemical reaction between chitosan and formalin as follows [10, 12, 15]:

$$\Delta n_{\text{sens}} = n_{\text{sens}}^d - n_{\text{sens}} = \left( n_{\text{sens}} + C_a \frac{dn}{dc} \right) - n_{\text{sens}} = C_a \frac{dn}{dc}$$

(2)

where $n_{\text{sens}}^d$ is the refractive index of the sensing dielectric medium after adsorption of formaldehyde molecules, $n_{\text{sens}}$ is the refractive index of the sensing dielectric medium before adsorption of formaldehyde molecules and is equal to the refractive index of PBS saline, $C_a$ is the concentration of adsorbed biomolecules for example 1000 nM formaldehyde solution, and $dn/dc$ is the refractive index increment factor. For PBS, the increment factor is 0.181 cm$^3$/gm [12, 16, 18, 51]. If a change in the SPR angle is found, a change in the propagation constant of SPW has been found which is explained mathematically in [10] as given below:

$$K_{\text{SPW}} = \frac{2\pi}{\lambda} n_{\text{prim}} \sin \theta_{\text{SPR}}$$

(3)

Finally, $F_{\text{SPR}}$ is changed due to the change in the propagation constant of SPW which can be explained by the following equation [10, 16, 18]:

$$F_{\text{SPR}} = \frac{K_{\text{SPW}} C_a}{2\pi n_{\text{eff}}}$$

(4)

where $C_a/n_{\text{eff}}$ is the propagation velocity of SPW that is a perpendicularly confined evanescent electromagnetic wave [52–54]. If the SPR angle of optical wave is tuned, SPR condition is achieved, where reflectance ($R$) of reflected wave is the minimum and transmittance ($T$) is the maximum and then SPW penetrates at $F_{\text{SPR}}$ along the $x$-direction. We define two plots “transmittance versus surface resonance frequency ($T$–$F_{\text{SPR}}$ curve)” as well as “reflectance versus surface resonance angle ($R$–$\theta_{\text{SPR}}$ curve)” as surface resonance detecting attributors. To make these curves, we use Fresnel equation for the seven-layer hetero optical system to determine reflected and transmitted light intensities discussed elaborately in [9–12, 14, 21, 22].

3. Numerical results analysis

3.1 Formalin detection approach

In this paper, Formaldehyde is detected by interacting with Chitosan and biomolecular components. Therefore, when a chemical bond is formed with the probe which is attached to the target component, it forms additional bonding which shows peculiar phenomena. From the response of the phenomena, one can easily determine that the sample contains formalin or not. This section is based on the tabulated value of concentration for the minimum reflectance & SPR angle along with the SPR frequency and maximum transmittance which helps detect formalin successfully. Here, we discuss in detail how dose our proposed biosensor distinguish from the presence of formaldehyde in the sensing solution. Firstly, a numerical analysis is initiated by checking the $R$–$\theta_{\text{SPR}}$ and $T$–$F_{\text{SPR}}$ curves in the absence of both formalin (target ligand) and chitosan (probe ligand), as shown in Fig. 2. In our proposed SPR device, PBS is used as a sensing medium that helps measure the dependency of reflectance on $\theta_{\text{SPR}}$ and transmittance on $F_{\text{SPR}}$. The work is continued by assuming that our sensor is susceptible of differentiating between probe element (chitosan) and detectable target (formalin) with regard to the analysis of detection. It is noticeable that an increase in the SPR angle and SPR frequency towards the right side of $R$–$\theta_{\text{SPR}}$ and $T$–$F_{\text{SPR}}$ curve is found due to the use of nano film TiO$_2$-SiO$_2$ layers, whose phenomenon accounts for enhanced sensitivity [39].

Figures 2(a) and 2(b) illustrate the $R$–SPR angle and $T$–$F_{\text{SPR}}$ curve. The blue line in Figs. 2(a) and 2(b) shows the SPR angle (56.26°) and $F_{\text{SPR}}$ (97.968 THz) during both probe (chitosan) and target (formalin), which are absent respectively in the sensor. The SPR
angle and $F_{\text{SPR}}$ of bare sensor are 56.26° and 97.968 THz, respectively. The red line in Fig. 2(a) shows the SPR angle (56.34°) and the green line in Fig. 2(b) shows $F_{\text{SPR}}$ (98.688 THz), while 1000nM probe (chitosan) is presented in PBS.

Secondly, we observe the change of detecting attributes ($\Delta \theta_{\text{SPR}}$ & $R_{\text{min}}$) and ($\Delta F_{\text{SPR}}$ & $T_{\text{max}}$) due to adding different concentrated formalin as shown in Fig. 3, and these changed are provided in Table 2. The data of Table 2 are extracted from Figs.3(a) and 3(b), respectively.

Table 2 Data of detecting attributors $R_{\text{min}}$ (%), $\theta_{\text{SPR}}$ (deg), $T_{\text{max}}$ (dB) and $F_{\text{SPR}}$ (THz) for different concentrated formalin ranging from 1000nM to 1200nM.

| Concentration            | $R_{\text{min}}$ (%) | $\theta_{\text{SPR}}$ (°) | $T_{\text{max}}$ (dB) | $F_{\text{SPR}}$ (THz) |
|--------------------------|-----------------------|-----------------------------|-----------------------|------------------------|
| 1000 (Immobilizer probe) | 0.0044                | 56.3400                     | 0.3795                | 98.688                 |
| 1000 (Detectable target) | 0.0062                | 58.0500                     | 0.3981                | 99.875                 |
| 1001 (Detectable target) | 0.0066                | 58.3800                     | 0.4002                | 100.008                |
| 1010 (Detectable target) | 0.0070                | 58.6700                     | 0.4018                | 100.106                |
| 1100 (Detectable target) | 0.0082                | 59.4900                     | 0.4106                | 100.627                |
| 1110 (Detectable target) | 0.0085                | 59.6800                     | 0.4129                | 100.761                |
| 1200 (Detectable target) | 0.0100                | 60.6200                     | 0.4249                | 101.447                |

Since the change of concentration is due to the immobilization of chitosan within the sensing medium, the local refractive index of the sensing medium is also changed followed by (2). Equation (1) states that the SPR angle changes if $n_{\text{sens}}$ changes, which finally translates a change in $K_{\text{SPW}}$ observed from (3). At the transition point where the SPW...
wave vector and optic wave vector are equal, the minimum reflectance ($R_{\text{min}}$) and maximum transmittance ($T_{\text{max}}$) are found. As illustrated in Fig. 2, before reaction of formalin with chitosan on the sensor device, no significant change occurs in the SPR angle ($\Delta \theta_{\text{SPR}} = 0.080^\circ$) and frequency ($\Delta F_{\text{SPR}} = 0.72$ THz) due to no bonding reaction between the probe ligand and sensing target.

Based on chemical bonding between the probe ligand and sensing target, the chemical bonding configuration is changing, which leads to a change in the optical properties of the interface. If the concentration of formalin is increased, it forms more bonds with probe thus indicating greater interaction with the sensing target. The chemical bonding between the probe ligand and sensing target.

In the detection style, firstly, we found out the threshold values of ($\Delta R_{\text{min}}$) & ($\Delta \theta_{\text{SPR}}$) and ($\Delta F_{\text{SPR}}$) from Table 2 by using the (5).

$$
\begin{align*}
(\Delta R_{\text{min}})^{\text{Th}} &= R_{\text{Probe}} - R_{\text{Target}} \\
&= 0.0044 - 0.0062 = 0.0018 \quad (5a) \\
(\Delta \theta_{\text{SPR}})^{\text{Th}} &= \theta_{\text{Probe}} - \theta_{\text{Target}} \\
&= 56.340 - 58.050 = 1.71 \quad (5b) \\
(\Delta F_{\text{SPR}})^{\text{Th}} &= F_{\text{Probe}} - F_{\text{Target}} \\
&= 98.688 - 99.875 = 1.187 \quad (5c)
\end{align*}
$$

where $R_{\text{Probe}}$ represents the minimum reflectance of probe ligand (chitosan), $R_{\text{Target}}$ denotes the minimum reflectance of sampling target, $\theta_{\text{Probe}}$ depicts the SPR angle of probe ligand, and $\theta_{\text{Target}}$ is the SPR angle of sampling target. We reach the same conclusion by taking $\Delta F_{\text{SPR}}$ and $\Delta T_{\text{max}}$ also as the detecting attributes.

Then we determine the change of the minimum reflectance, change of SPR angle, change of maximum transmittance, and change of $F_{\text{SPR}}$ for different concentrated formalin molecules by using the data in Table 2 and tabulated them into Table 3.

| Concentration (C) (nM) | $\Delta R_{\text{min}}$ | $\Delta \theta_{\text{SPR}}$ | $\Delta F_{\text{SPR}}$ |
|------------------------|------------------------|------------------------|------------------------|
| 1000 (Target)          | 0.0022                 | 2.04                   | 0.0207                 |
| 1001 (Target)          | 0.0026                 | 2.33                   | 0.0223                 |
| 1100 (Target)          | 0.0038                 | 3.15                   | 0.0311                 |
| 1110 (Target)          | 0.0041                 | 3.34                   | 0.0334                 |
| 1200 (Target)          | 0.0056                 | 4.28                   | 0.0354                 |

Table 3 | Change of $\Delta R_{\min}^{\text{Th}}$, $\Delta T_{\max}^{\text{Th}}$, $\Delta F_{\text{SPR}}^{\text{Th}}$, and $\Delta \theta_{\text{SPR}}^{\text{Th}}$ values from (5) for different concentrations of dielectric formalin.

Table 4 Four probable conditions for making decision about successful interaction.

| Conditions for using $\theta_{\text{SPR}}$ & $T_{\text{max}}$ as detecting attribute | Conditions for using $F_{\text{SPR}}$ & $T_{\text{max}}$ as detecting attribute | Judgement |
|-------------------------------------------|-------------------------------------------|-------------------------|
| $\Delta R_{\text{min}}$ $\geq$ $\Delta R_{\text{min}}$ | $\Delta \theta_{\text{SPR}}$ $\geq$ $\Delta \theta_{\text{SPR}}$ | $\Delta F_{\text{SPR}}$ $\geq$ $\Delta F_{\text{SPR}}$ |
| $\Delta T_{\min}$ $\geq$ $\Delta T_{\max}$ | $\Delta F_{\text{SPR}}$ $\leq$ $\Delta F_{\text{SPR}}$ | Formalin is detected |
| $\Delta T_{\max}$ $\leq$ $\Delta T_{\max}$ | $\Delta \theta_{\text{SPR}}$ $\leq$ $\Delta \theta_{\text{SPR}}$ | $\Delta F_{\text{SPR}}$ $\leq$ $\Delta F_{\text{SPR}}$ | Reevaluate |
| $\Delta R_{\min}$ $\leq$ $\Delta R_{\max}$ | $\Delta \theta_{\text{SPR}}$ $\leq$ $\Delta \theta_{\text{SPR}}$ | $\Delta F_{\text{SPR}}$ $\leq$ $\Delta F_{\text{SPR}}$ | Reevaluate |
| $\Delta R_{\max}$ $\leq$ $\Delta R_{\max}$ | $\Delta \theta_{\text{SPR}}$ $\geq$ $\Delta \theta_{\text{SPR}}$ | $\Delta F_{\text{SPR}}$ $\geq$ $\Delta F_{\text{SPR}}$ | Free probe |
If the measured values are greater than these threshold parameters, we observe the presence of formalin in that target sample. For clarifying detection conditions, we reach a conclusion according to Table 4. These values can really give an idea about successful interaction or the failed ones. The first condition in Table 4 expresses the desired condition, the second and third ones need careful recheck for attaining desired condition, and the fourth condition confirms that the probe is still free a target molecule.

3.2 Effect of different layers on sensor sensitivity

The sensor’s performance is evaluated in terms of sensitivity ($S$) which is defined as [16, 18]:

$$S = \frac{\Delta \theta_{\text{SPR}}}{\Delta n_{\text{sens}}} = \frac{\Delta \theta_{\text{SPR}}}{C_a \frac{dn}{dc}} \tag{6}$$

where $\Delta \theta_{\text{SPR}}$ is the change of SPR angle due to the presence of formalin, and $\Delta n_{\text{sens}}$ is the change of refractive index of the sensing dielectric after adsorption of formaldehyde molecules described in (2). The SPR angle shifts rightward in the SPR curve with the increment of refractive index followed by (1).

At the SPR point, the optical wave propagation constant which is represented by (3) must be equal to the surface wave propagation constant. It is known from (3) that the surface plasmon propagation constant changes according to the change of refractive index of sensing medium. Finally, it is observed that the SPR angle changing characteristics is responsible for the change of refractive index of sensing medium.

Firstly, in this section, we discuss the effect of inserting different layers on the detecting attributors such as the change of SPR angle and SPR frequency in the sensor configuration. Figs. 4(a) and 4(b) show the minimum reflectance ($R_{\text{min}}$) vs. SPR angle ($\theta_{\text{SPR}}$) and the maximum transmittance ($T_{\text{max}}$) vs. $F_{\text{SPR}}$ curves for different structures including the conventional structure and proposed structure at the refractive index $n_{\text{sens}}=1.34$ RIU (bare sensor). Figure 4 shows that the SPR angle and SPR frequency for the conventional layer biosensor are $54.36^\circ$ and $94.1547$ THz, respectively. Again, Fig. 4 shows that the SPR angle and SPR frequency with the graphene and gold metal layer based biosensor are $54.57^\circ$ and $94.4015$ THz, respectively. In this case, it can easily be observed that the change of SPR angle and SPR frequency for the conventional structure is very poor whereas the sensitivity with graphene but without TiO$_2$, SiO$_2$, and MoS$_2$ layers is consistently better than the conventional structure. This is due to the electron loss of graphene, which is accompanying with the imaginary dielectric constant. This increased SPR angle will lead to obtaining increased sensitivity of the sensor as sensitivity is directly proportional to the variation of the SPR angle discussed in [42–44] according to (6). Furthermore, Fig. 4 shows that the SPR angle and SPR frequency without TiO$_2$, SiO$_2$, and graphene but with MoS$_2$ layer are $55.60^\circ$ and $95.5935$ THz, respectively. This is because of MoS2’s larger band gap [11, 18, 22, 42, 43], higher optical absorption efficiency [22–24], and larger work function (5.1 eV) as compared with graphene [11]. Further again, if both graphene and MoS$_2$ are used and TiO$_2$ and SiO$_2$ layers are not used, then Fig. 4 shows that the SPR angle and SPR frequency are $55.86^\circ$ and $96.2495$ THz, respectively. This is greater than the performance of using other materials due to the present of both characteristics of graphene and MoS2. Furthermore, if the TiO$_2$-SiO$_2$ composite layer is used with the graphene and MoS$_2$, Fig. 4 shows that the SPR angle and SPR frequency are $55.90^\circ$ and $96.9236$ THz, respectively. Since TiO$_2$ and SiO$_2$ have a purely real refractive index, they can be used as an adherence layer above the prism base. As an adherence layer, the composite layer performs better than the individual TiO$_2$ and SiO$_2$ [16, 18] do because rich plasmon happens at the TiO$_2$-SiO$_2$ interface [18]. And this plasmon enhances light trapping effectively [32] which will generate more
surface plasmons (SPs). More surface plasmons (SPs) will enhance the SPR angle rightwards. An increase in the SPR angle will increase the SPR sensitivity. Lastly, the SPR angle and SPR frequency for the proposed structure are 56.26° and 97.968 THz, respectively, which reach the highest values among all the previous structures. Addition of probe molecules shifts the SPR angle rightwards due to the change of refractive index of the sensing dielectric. By adsorption of immobilized ions, an electron rich molecule would change in the sensing layer concentration which has led to a variation of the propagation constant.

\[
\theta_{\text{SPR}} = \frac{\Delta \theta_{\text{SPR}}}{\Delta \text{RIU}}
\]

Equation (2) shows how the SPR angle changes due to the change of molarity of the solution and refractive index. By this calibration, one can directly know the SPR angle of the system, just by measuring the refractive index (RI) of the sensing solution. The variation of the reflection intensity in accordance with the incident angle is plotted in Fig. 5. The reflectance curves at 1.34 RIU of sensing medium refractive index (bare sensor) and 1.41 RIU (present of formalin in sensor) are presented by solid and dashed lines of different colors, respectively. Here, the proposed structure (with all layers) is compared with some other structures including firstly the structure without TiO$_2$, SiO$_2$, MoS$_2$, and graphene layers (conventional structure), secondly the structure without TiO$_2$, SiO$_2$, and MoS$_2$ layers, thirdly the structure without TiO$_2$, SiO$_2$, and graphene layers, fourthly the structure without TiO$_2$ and SiO$_2$, fifthly the structure without TiO$_2$ layer, and finally the structure without SiO$_2$. The resonance angle (\(\theta_{\text{SPR}}\)) at 1.34 RIU and 1.41 RIU of the sensing layer is calculated and then the sensitivity is measured. One can easily observe from Fig. 4 that the sensitivity increases gradually in accordance with the adding layers and it reaches the maximum with the hybrid structure of seven layers (proposed structure).

Thirdly, in this section, the shift of the SPR angle with the increment of refractive index having
a step size $\delta C_n = 0.01$ is measured and the corresponding increment of sensitivity of the proposed biosensor according to the (6) is also determined and graphically shown in Fig. 6.

![Graph showing the variation of reflection intensity with respect to the incidence angle for different SPR sensor structures.](image1.png)

**Fig. 5** Variation of the Reflection Intensity with respect to the incidence angle for different structures of SPR sensor.

![Graph showing the sensitivity percentage vs. refractive index curve for different structures.](image2.png)

**Fig. 6** Percentage of sensitivity vs. refractive index curve for different structures proposed.

From Fig. 6, firstly it is observed that the sensitivity for the conventional structure ranges from 70.44% to 75.375% with respect to the sensing medium refractive index ranging $n_{\text{sens}}^d = 1.34$ RIU to $n_{\text{sens}}^d = 1.41$ RIU, respectively. After then the sensitivity of the proposed structure with graphene but without TiO$_2$-SiO$_2$ and MoS$_2$ is investigated and it equals to a range from 71.62% to 76.375%, which is comparatively better than the conventional structure. Furthermore, the sensitivity of the structure with MoS$_2$ but without TiO$_2$-SiO$_2$ and graphene covers a range from 76.44% to 81.375%.

If both graphene and MoS$_2$ are used and TiO$_2$-SiO$_2$ are not used, the sensitivity is more improved than the previous structures whose sensitivity covers from 77% to 82.625%. Now, if the SiO$_2$ layer is used with graphene and MoS$_2$ and TiO$_2$ is not used, the sensitivity enhances to a range from 78% to 85.00%.

If a TiO$_2$ layer is used instead of the SiO$_2$ layer in previous structures, just like before the sensitivity keeps almost constant. If we use all the layers at a time, which is a proposed structure in this work, the sensitivity is the highest among all the previous structures, which covers the range from 79% to 85.375%. Finally, in this section, the sensitivities for different structures are summarized in Table 5.

| Model structure                        | Sensitivity (%RIU$^{-1}$) |
|----------------------------------------|---------------------------|
| Without TiO$_2$, SiO$_2$, MoS$_2$, and graphene | 75.26                     |
| Without TiO$_2$, SiO$_2$, and MoS$_2$, and with graphene | 76.24                     |
| Without TiO$_2$, SiO$_2$, and graphene, and with MoS$_2$ | 81.82                     |
| With graphene and MoS$_2$ and without TiO$_2$ & SiO$_2$ | 82.40                     |
| With graphene, SiO$_2$ & MoS$_2$, and without TiO$_2$ | 85.14                     |
| With graphene, TiO$_2$ & MoS$_2$, and without SiO$_2$  | 82.10                     |
| With graphene-MoS$_2$-TiO$_2$-SiO$_2$ (proposed) | 85.375                   |

### 3.5 References

In this paper, a numerical analysis is investigated to notice the consequence of adding of graphene, MoS$_2$, TiO$_2$, and SiO$_2$ layers step by step on sensitivity parameters for formalin detection. The first concern of this study is to detect the presence of the formalin based on the ATR method by noting the change of “SPR angle versus minimum reflectance” attributor and “$F_{\text{SPR}}$ versus maximum transmittance” attributor. In this paper, chitosan is used as a probe legend to react with formalin (formaldehyde). The second concern is the sensitivity analysis by adding of graphene, MoS$_2$, TiO$_2$, and SiO$_2$ layers step by step. Graphene as well as MoS$_2$ thin films plays an important role in developing electro-optical sensor device due to their biocompatibility, high surface to volume ratio, low isoelectric point, and better chemical stability properties, which makes it very suitable for applications like formalin detection. For plasmonic effect near TiO$_2$-SiO$_2$ interface, the light
trapping is effectively enhanced because the enhanced light trapping more surface plasmons is generated which will eventually enhance the resonance angle, which can indeed satisfy the maximum sensitivity requirement. Numerically, the sensitivity of 85.375% with a refractive index of 1.41 RIU has been observed for the proposed sensor.

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