Multiuser Media-based Modulation for Massive MIMO Systems

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Abstract—Media-based modulation (MBM) is an attractive modulation scheme which is getting increased research attention recently. In this paper, we consider MBM for the uplink of a massive MIMO system, which has not been reported before. Each user is equipped with one transmit antenna with multiple radio frequency (RF) mirrors (parasitic elements) placed near it. The base station (BS) is equipped with tens to hundreds of receive antennas. We investigate the potential performance advantage of multiuser MBM (MU-MBM) in a massive MIMO setting. Our results show that multiuser MBM (MU-MBM) can significantly outperform other modulation schemes. For example, a bit error performance achieved using 500 receive antennas at the BS in a massive MIMO system using conventional modulation can be achieved using just 128 antennas using MU-MBM. Even multiuser spatial modulation and generalized spatial modulation in the same massive MIMO settings require more than 200 antennas to achieve the same bit error performance. Also, recognizing that the MU-MBM signal vectors are inherently sparse, we propose an efficient MU-MBM signal detection scheme that uses compressive sensing based reconstruction algorithms like orthogonal matching pursuit (OMP), compressive sampling matching pursuit (CoSaMP), and subspace pursuit (SP).

Keywords — Media-based modulation, RF mirrors, massive MIMO, sparse recovery, OMP, CoSaMP, subspace pursuit.

I. INTRODUCTION

Media-based modulation (MBM), a promising modulation scheme for wireless communications in multipath fading environments, is attracting recent research attention [1]-[5]. The key features that make MBM different from conventional modulation are: i) MBM uses digitally controlled parasitic elements external to the transmit antenna that act as radio frequency (RF) mirrors to create different channel fade realizations, which are used as the channel modulation alphabet, and ii) it uses indexing of these RF mirrors to convey additional information bits. The basic idea behind MBM can be explained as follows.

Placing RF mirrors near a transmit antenna is equivalent to placing scatterers in the propagation environment close to the transmitter. The radiation characteristics of each of these scatterers (i.e., RF mirrors) can be changed by an ON/OFF control signal applied to it. An RF mirror reflects back the incident wave originating from the transmit antenna or passes the wave depending on whether it is OFF or ON. The ON/OFF status of the mirrors is called as the ‘mirror activation pattern’ (MAP). The positions of the ON mirrors and OFF mirrors change from one MAP to the other, i.e., the propagation environment close to the transmitter changes from one MAP to the other MAP. Note that in a rich scattering environment, a small perturbation in the propagation environment will be augmented by many random reflections resulting in an independent channel. The RF mirrors create such perturbations by acting as controlled scatterers, which, in turn, create independent fade realizations for different MAPs.

If \( m_{rf} \) is the number of RF mirrors used, then \( 2^{m_{rf}} \) MAPs are possible. If the transmitted signal is received through \( n_r \) receive antennas, then the collection of \( 2^{m_{rf}} \cdot n_r \)-length complex channel gain vectors form the MBM channel alphabet. This channel alphabet can convey \( m_{rf} \) information bits through MAP indexing. If the antenna transmits a symbol from a conventional modulation alphabet denoted by \( \Lambda \), then the spectral efficiency of MBM is \( \eta_{mbm} = m_{rf} + \log_2 |\Lambda| \) bits per channel use (bpcu). An implementation of a MBM system consisting of 14 RF mirrors placed in a compact cylindrical structure with a dipole transmit antenna element placed at the center of the cylindrical structure has been reported in [3]. Note that RF mirrors are just digitally controlled parasitic elements (e.g., capacitors, varactors or switched capacitors) and they are not driven by RF chains and power amplifiers. Early reporting of the idea of using parasitic elements for index modulation purposes (in the name ‘aerial modulation’) can be found in [6],[7].

MBM has been shown to possess attractive performance attributes, particularly when the number of receive antennas is large [1]-[5]. Specifically, MBM with \( n_r \) receive antennas over a multipath channel has been shown to asymptotically achieve the capacity of \( n_r \) parallel AWGN channels [2]. This suggests that MBM can be attractive for use in massive MIMO systems which typically employ a large number of receive antennas at the BS. However, the literature on MBM so far has focused mainly on single-user (point-to-point) communication settings. Our first contribution in this paper is that, we report MBM in multiuser massive MIMO settings and demonstrate significant performance advantages of MBM compared to conventional modulation. For example, a bit error performance achieved using 500 receive antennas at the BS in a massive MIMO system using conventional modulation can be achieved using just 128 antennas with multiuser MBM. Even multiuser spatial modulation (SM) and generalized spatial modulation (GSM) [8]-[12] in the same massive MIMO settings require more than 200 antennas to achieve the same bit error performance. This suggests that multiuser MBM can be an attractive scheme for use in the uplink of massive MIMO systems.

The second contribution relates to exploitation of the inherent sparsity in multiuser MBM signal vectors for low-complexity signal detection at the BS receiver. We resort to compressive sensing (CS) based sparse recovery algorithms for this purpose. Several efficient sparse recovery algorithms are known in the literature[13]-[15]. We propose a multiuser MBM signal detection scheme that employs greedy sparse recovery algorithms like orthogonal matching

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pursuit (OMP)[13], compressive sampling matching pursuit (CoSaMP) [14], and subspace pursuit (SP)[15]. The results demonstrate that CS based sparse signal recovery approach is a natural and efficient approach for multiuser MBM signal detection in massive MIMO systems.

The rest of the paper is organized as follows. The MU-MBM system model is introduced in Sec. II. The performance of MU-MBM with maximum likelihood detection is presented in Sec. III. The proposed sparsity-exploiting detection scheme for MU-MBM signal detection and its performance in massive MIMO systems are presented in Sec. IV. Conclusions are presented in Sec. V.

II. MULTIUSER MBM SYSTEM MODEL

Consider a massive MIMO system with $K$ uplink users and a BS with $n_r$ receive antennas (see Fig. 1), where $K$ is in the tens (e.g., $K = 16, 32$) and $n_r$ is in the hundreds ($n_r = 128, 256$). The users employ MBM for signal transmission. Each user has a single transmit antenna and $m_r$ RF mirrors placed near it. In a given channel use, each user selects one of the $2^{m_r} \cdot 2^{\log n_r}$ mirror activation patterns (MAPs) using $m_r$ information bits. A mapping is done between the combinations of $m_r$ information bits and the MAPs. This mapping is made known a priori to both transmitter and receiver for encoding and decoding purposes, respectively.

A. Single-user MBM channel alphabet

The MBM channel alphabet of a single user is the set of all channel gain vectors corresponding to the various MAPs of that user. Let us define $\mathcal{M} = \{2^{m_r}\}$, where $M$ is the number of possible MAPs corresponding to $m_r$ RF mirrors. Let $\mathbf{h}_k^m$ denote the $n_r \times 1$ channel gain vector corresponding to the $m$th MAP of the $k$th user, where $\mathbf{h}_k^m = [h_{1,k}^m \ h_{2,k}^m \ \cdots \ h_{n_r,k}^m]^T$, $h_{i,k}^m$ is the channel gain corresponding to the $m$th MAP of the $k$th user to the $i$th receive antenna, $i = 1, \ldots, n_r$, $k = 1, \ldots, K$, and $m = 1, \ldots, M$, and the $h_{i,k}^m$s are assumed to be i.i.d. and distributed as $\mathcal{CN}(0, 1)$. The MBM channel alphabet for the $k$th user, denoted by $\mathbb{H}_k$, is then the collection of these channel gain vectors, i.e., $\mathbb{H}_k = \{\mathbf{h}_k^1, \mathbf{h}_k^2, \ldots, \mathbf{h}_k^M\}$. The MBM channel alphabet of each user is estimated a priori at the BS receiver through pilot transmission.

B. Single-user MBM signal set

Define $\mathbb{A}_q \triangleq \mathbb{A} \cup 0$. The single-user MBM signal set, denoted by $\mathcal{S}_{\text{SU-MBM}}$, is the set of $M \times 1$-sized MBM signal vectors given by

$$\mathcal{S}_{\text{SU-MBM}} = \{\mathbf{s}_{m,q} \in \mathbb{A}_q : m = 1, \ldots, M, q = 1, \ldots, |\mathbb{A}|\} \quad \text{s.t.} \quad \mathbf{s}_{m,q} = [s_{m,q,0} \ s_{m,q,1} \ 0 \cdots 0]^T, s_q \in \mathbb{A},$$

where $m$ is the index of the MAP. That is, an MBM signal vector $\mathbf{s}_{m,q}$ in (2) means a complex symbol $s_q \in \mathbb{A}$ being transmitted on a channel with an associated channel gain vector $\mathbf{h}^m$, where $\mathbf{h}^m$ is the $n_r \times 1$ channel gain vector corresponding to the $m$th MAP. Therefore, the $n_r \times 1$ received signal vector corresponding to a transmitted MBM signal vector $\mathbf{s}_{m,q}$ can be written as

$$\mathbf{y} = s_q \mathbf{h}^m + \mathbf{n},$$

where $\mathbf{n} \in \mathbb{C}^{n_r}$ is the AWGN noise vector with $\mathbf{n} \sim \mathcal{CN}(0, \sigma^2 I)$. The size of the single-user MBM signal set is $|\mathcal{S}_{\text{SU-MBM}}| = |\mathbb{A}|$. For example, if $m_r = 2$ and $|\mathbb{A}| = 2$ (i.e., BPSK), then $|\mathcal{S}_{\text{SU-MBM}}| = 8$, and the corresponding MBM signal set is given by

$$\mathcal{S}_{\text{SU-MBM}} = \{[1,0,0,1,0,1,1,0]^T, 0,0,0,0,0,0,0,0]^T\}.$$  

C. Multiuser MBM received signal

With the above definitions of single-user MBM channel alphabet and signal set, the multiuser MBM signal set with $K$ users is given by $\mathcal{S}_{\text{MU-MBM}} = \mathcal{S}_{\text{SU-MBM}}^K$. Let $\mathbf{x}_k \in \mathcal{S}_{\text{SU-MBM}}$ denote the transmit MBM signal vector from the $k$th user. Let $\mathbf{H} = [\mathbf{H}_1 \ \mathbf{H}_2 \ \cdots \ \mathbf{H}_K]$ denote the channel gain matrix given by $\mathbf{H} = [\mathbf{h}_1 \mathbf{h}_2 \cdots \mathbf{h}_K] \in \mathbb{C}^{n_r \times KM}$, and $\mathbf{h}_k^m$ is the channel gain vector of the $k$th user corresponding to $m$th MAP as defined before. The $n_r \times 1$ multiuser received signal vector at the BS is then given by

$$\mathbf{y} = \mathbf{H} \mathbf{x} + \mathbf{n},$$

where $\mathbf{n}$ is the $n_r \times 1$ AWGN noise vector with $\mathbf{n} \sim \mathcal{CN}(0, \sigma^2 I)$.
III. ML DETECTION PERFORMANCE OF MU-MBM

In this section, we present the BER performance of multiuser MBM under maximum likelihood (ML) detection and compare with the performances of other multiuser schemes that employ conventional modulation, spatial modulation, and generalized spatial modulation. The ML detection rule for the multiuser MBM system model in (5) is given by

$$\hat{x} = \arg\min_{x \in \mathbb{C}^{M \times M_{\text{RF}}}} \|y - Hx\|^2. \quad (6)$$

We consider a MU-MBM system with $K = 2$, $n_r = 8$, $m_{rf} = 3$, BPSK, and 4 bpcu per user. Let $n_t$ and $n_{rf}$ denote the number transmit antennas and transmit RF chains, respectively, at each user. Note that in the considered MU-MBM system, each user uses one transmit antenna and one transmit RF chain, i.e., $n_t = n_{rf} = 1$. We compare the performance of the above MU-MBM system with those of three other multiuser systems which use (i) conventional modulation (CM), (ii) spatial modulation (SM), and (iii) generalized spatial modulation (GSM). The multiuser system with conventional modulation (MU-CM) uses $n_t = n_{rf} = 1$ at each user and employs 16-QAM to achieve the same spectral efficiency of 4 bpcu per user. The multiuser system with SM (MU-SM) uses $n_t = 2$, $n_{rf} = 1$, and 8-QAM, achieving a spectral efficiency of $\log_2 n_t + \log_2 |\mathcal{A}| = \log_2 2 + \log_2 8 = 4$ bpcu per user. The multiuser system with GSM (MU-GSM) uses $n_t = 4$, $n_{rf} = 2$, and BPSK, achieving a spectral efficiency of $\lfloor \log_2 (2^{n_r}) \rfloor + \log_2 |\mathcal{A}| = \lfloor \log_2 (2^4) \rfloor + \log_2 2 = 4$ bpcu per user.

Figure 2 shows the BER performance of the MU-MBM, MU-CM, MU-SM, and MU-GSM systems described above. The following inferences can be drawn from Fig. 2:

- The MU-MBM system achieves the best performance among all the four systems considered. For example, MU-MBM performs better by about 5 dB, 4 dB, 2.5 dB compared to MU-CM, MU-SM, and MU-GSM systems, respectively, at a BER of $10^{-5}$.
- The better performance of MU-MBM can be attributed to more bits being conveyed through mirror indexing, which allows MU-MBM to use lower-order modulation alphabets (BPSK) compared to other systems which may need higher-order alphabets (8-QAM, 16-QAM) to achieve the same spectral efficiency.
- MU-MBM performs better than MU-GSM though both use BPSK in this example. This can be attributed to the good distance properties of the MBM signal set [2].

Note that though the results in Fig. 2 illustrate the performance superiority of MU-MBM over MU-CM, MU-SM, and MU-GSM, they are presented only for a small system with $K = 2$ and $n_r = 8$. This is because ML detection is prohibitively complex for systems with large $K$ (ML detection is exponentially complex in $K$). However, massive MIMO systems are characterized by $K$ in the tens and $n_r$ in the hundreds. Therefore, low-complexity detection schemes which scale well for such large-scale MU-MBM systems are needed. To address this need, we resort to exploiting the inherent sparse nature of the MBM signal vectors, and devise a compressive sensing based detection algorithm in the following section.

IV. SPARSITY-EXPLOITING DETECTION OF MU-MBM SIGNALS

It is evident from the example signal set in (4) that the MBM signal vectors are inherently sparse. An MBM signal vector has only one non-zero element out of $M$ elements, leading to a sparsity factor of $1/M$. For example, consider an MBM signal set with $m_{rf} = 4$ and $M = 2^m_{rf} = 16$. Out of 16 elements in a signal vector, only one element is non-zero resulting in a sparsity factor of $1/16$. Exploitation of this inherent sparsity to devise detection algorithms can lead to efficient signal detection at low complexities. Accordingly, we propose a low-complexity MU-MBM signal detection scheme that employs compressive sensing based sparse reconstruction algorithms like OMP, CoSaMP, and SP.

A. Proposed sparsity-exploiting detection algorithm

We first model the MU-MBM signal detection problem as a sparse reconstruction problem and then employ greedy algorithms for signal detection. Sparse reconstruction is concerned with finding an approximate solution to the following problem

$$\min_{x} \|x\|_0 \text{ subject to } y = \Phi x + n, \quad (7)$$

where $\Phi \in \mathbb{C}^{m \times n}$ is called the measurement matrix, $x \in \mathbb{C}^n$ is the complex input signal vector, $y \in \mathbb{C}^m$ is the noisy observation corresponding to the input signal, and $n \in \mathbb{C}^m$ is the complex noise vector. The MU-MBM signal detection problem at the BS in (5) can be modeled as a sparse recovery problem in (7), with the measurement matrix being the channel matrix $H \in \mathbb{C}^{m_r \times K M}$, the noisy observation being the received signal vector $y \in \mathbb{C}^m$, and the input being the MU-MBM transmit signal vector $x \in \mathbb{C}^{M_{\text{RF}} \times M_{\text{RF}}}$. The noise vector is additive complex Gaussian with $n \sim \mathcal{CN}(0, \sigma^2 I)$.

Algorithm 1 shows the listing of the pseudo-code of the proposed sparsity-exploiting detection algorithm for MU-MBM signals. Here, SR denotes the sparse recovery algorithm, which can be any one of OMP, CoSaMP, and SP. The signal vector reconstructed by the sparse recovery algorithm is denoted by $\hat{x}_r$. Detecting the MU-MBM signal vector involves detecting the MBM signal vector transmitted by each user. An MBM signal vector from a user has exactly one non-zero entry out of $M$ entries as observed in the example MBM.
sparsity factors in MU-MBM, MU-SM, and MU-GSM. From Fig. 3, we observe that the proposed algorithm with OMP, CoSaMP, and SP achieve significantly better performance compared to MMSE. Among the three algorithms, CoSaMP and SP give the best performance. This illustrates the superior reconstruction/detection advantage of the proposed algorithm with SP. We will use the proposed algorithm with SP in the subsequent performance results figures. It is noted that, for an $m \times n$ matrix and a $k$-sparse vector, the complexity of SP is $O(kmn)$ [15], where as the complexity of MMSE detection is $O(k^3)$. **Performance of MU-MBM, MU-SM, MU-GSM:**

Figure 4 shows a BER performance comparison between MU-MBM, MU-SM, MU-GSM, and MU-GSM in a massive MIMO setting with $K = 16$ and $n_r = 128$. The proposed algorithm with SP is used for detection in MU-MBM, MU-SM, and MU-GSM. ML detection is used for MU-CM. The spectral efficiency is fixed at 5 bpcu per user for all the four schemes. MU-MBM achieves this spectral efficiency with $n_t = 1$, $n_r = 1$, $n_r = 3$, and 4-QAM. MU-CM uses $n_t = 1$, $n_r = 1$, and 32-QAM to achieve 5 bpcu per user. To achieve the same 5 bpcu per user, MU-SM uses $n_t = 4$, $n_r = 1$, and 8-QAM, and MU-GSM uses $n_t = 5$, $n_r = 2$, and BPSK. The sparsity factors in MU-MBM, MU-SM, and MU-GSM.
are 1/8, 1/4, and 2/5, respectively. It can be seen that, MU-MBM clearly outperforms MU-CM, MU-SM, and MU-GSM. For example, at a BER of $10^{-5}$, MU-MBM outperforms MU-CM, MU-GSM, and MU-SM by about 7 dB, 5 dB, and 4 dB, respectively. The performance advantage of MU-MBM can be mainly attributed to its better signal distance properties [2]. MU-MBM is also benefited by its lower sparsity factor as well as the possibility of using lower-order QAM size because of additional bits being conveyed through indexing mirrors.

**Effect of number of BS receive antennas:**

Figure 5 shows an interesting result which demonstrates MU-MBM, MU-SM, MU-CM, and MU-GSM as a function of $n_r$ in a massive MIMO setting with $K = 16$, 5 bpcu per user, and SNR = 4 dB.

**OMP, CoSaMP, and subspace pursuit.** The proposed detection scheme was shown to achieve very good performance (e.g., significantly better performance compared to MMSE detection) at low complexity, making it suited for multuser MBM signal detection in massive MIMO systems. Channel estimation, effect of imperfect knowledge of the channel alphabet at the receiver, and effect of spatial correlation are interesting topics for further investigation.

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