Physico-Chemical Properties of NaV$_3$O$_8$ Prepared by Solid-State Reaction

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Abstract: Sodium–vanadium oxide NaV$_3$O$_8$ is synthesized via solid-state method and optimum synthesis conditions are chosen based on the data of DSC and TG analysis. The material synthesized is characterized by X-ray phase analysis, Raman spectroscopy and scanning electron microscopy. The ratio V$^{4+}$/V$^{5+}$ in the sample obtained is determined by X-ray photoelectron spectroscopy. Conductivity of the material synthesized was measured by impedance spectroscopy, pulse photometry and DC method over the range RT–570 $^\circ$C. It is shown that NaV$_3$O$_8$ has rather high conductivity essentially in type (6.3 $\times$ 10$^{-2}$ at room temperature). AC and DC conductivity measurements are performed and cycling of symmetric NaV$_3$O$_8$ $|$ Na$_3$Zr$_{1.85}$Nb$_{0.15}$Si$_3$O$_{12}$ $|$ NaV$_3$O$_8$ cell in galvanostatic conditions. Thermal stability is studied across 25–570 $^\circ$C temperature range. The results obtained are compared with the properties of NaV$_3$O$_8$ produced via aqueous solution.

Keywords: sodium power sources; cathode materials; sodium–vanadium oxides; solid state synthesis

1. Introduction

Lithium and lithium-ion batteries (LIBs) rank high among electrochemical power sources nowadays, because they deliver high specific energy and the highest working voltage. High-energy lithium-ion batteries show successful applications in low power equipment, such as consumer electronics. However, Li belongs to the rare metals, so the possibilities of extending the use of lithium-ion batteries to large equipment for power industry and electric vehicles will be restricted by the low availability of lithium raw materials. In this area, there is currently a lot of interest in developing power sources having characteristics close to those of LIBs but using easily available low-cost materials. Sodium and sodium-ion batteries (SIBs) are considered as materials that meet these requirements [1–3].

Sodium has a slightly smaller negative potential than lithium (−2.71 V versus −3.03 V), but at the same time it has a number of substantial advantages, the chief one being its almost inexhaustible resources in nature, easy regeneration and, as consequence, a lower cost of sodium batteries compared to lithium ones. Additionally, the majority of power sources with alkali-metal anodes use solutions of some inorganic salts in organic liquids as electrolytes. Such liquids are usually highly flammable, which creates safety issues due to a potential electrolyte leakage followed by its explosion or ignition. In this connection, moving away from liquid electrolytes and transition to all-solid-state power sources seems to be a very attractive option [4,5]. Solid electrolytes used in all-solid-state power sources are generally characterized by low conductivity; therefore, such power sources will deliver the best performance in devices operating at elevated temperatures. In view of this, designing efficient cathode materials stable at elevated temperatures (~300 $^\circ$C) is one of the basic areas in the development of all-solid-state power sources.

Application of vanadium oxides V$_m$O$_n$ (V$_2$O$_5$, V$_6$O$_{13}$, V$_6$O$_{14}$) [6] and their derivatives [7,8] as cathode materials of power sources has recently become the subject of intensive...
Both vanadium oxides and alkali metal vanadates are characterized by a layered structure formed by layers of vanadium–oxygen polyhedra [9]. There is enough space between the layers to allow the insertion of various cations, monovalent as well as polyvalent, which means that such compounds are capable of reversible intercalation of different ions. V–O bonds between the vanadium–oxygen layers are weak, which allows the layers to shift against each other and additionally increases the maximum possible amount of intercalated cations, i.e., the intercalation capacity of the material. The high theoretical capacity and energy density of vanadium oxides make them attractive cathode materials for power sources. Moreover, vanadium oxides and alkali metal vanadates often contain vanadium in lower oxidation states alongside $V^{5+}$ ions, which generates quite considerable electronic conductivity and, consequently, enhances the characteristics of the cathode material. Finally, vanadium oxides and their derivatives have an advantage of a relatively low cost. Thus, owing to the above-mentioned characteristics, vanadium oxides and alkali metal vanadates are attractive as cathode materials for power sources and are currently a subject of intensive research.

Cathodes based on vanadium oxides initially showed good performance in lithium and lithium-ion power sources [10,11]. Subsequently, with the growing interest in sodium power sources, sodium–vanadium oxides were proposed as cathode materials to be used in such batteries [12]. Studies into Na batteries with cathodes based on $NaV_6O_{15}$ [13], $Na_{0.33}V_2O_5$ [14] and $Na_{1.5+y}VO_3$ [15] confirmed the high potential of such materials and gave reason to continue investigating the compounds under discussion in terms of their possible application as active cathode materials of SIBs.

$NaV_3O_8$ is one of sodium–vanadium compounds currently attracting considerable scientific interest as a potential cathode material for sodium and sodium-ion power sources [16–19]. According to the literature data, Na-ion power sources with $NaV_3O_8$ cathode show a good performance in terms of specific energy. Thus, a cell with a sodium anode, an electrolyte of NaClO$_4$ solution in PC and a cathode containing $NaV_3O_8$ nanorods as active material delivered the reversible capacity of 162.1 mA·h·g$^{-1}$ and coulombic efficiency of 96% under the current density of 120 mA·g$^{-1}$ during 500 charge/discharge cycles. The reversible capacity of 88 mA·h·g$^{-1}$ is retained even at elevated current densities of about 2 A·g$^{-1}$ [15].

The available literature data indicate that the electrical characteristics of power sources with $NaV_3O_8$-based cathodes depend to a great extent on the morphology, particle size, crystallinity degree of the active cathode material and other factors, which, in their turn, depend on the technique by which the vanadate was initially synthesized [12]. Various methods of producing $NaV_3O_8$ have been proposed in the literature, e.g., it can be synthesized in the form of nanobelts [17], nanorods [19], or core/shell type nanoparticles [20], but these methods are long and complicated. In view of this, research into the physico-chemical properties and electrochemical behavior of $NaV_3O_8$ obtained through simple, traditional techniques is, no doubt, of great interest. Previously we have performed such experiments for $NaV_3O_8$ obtained by the method of aqueous solution [21]. Here we report on the results for $NaV_3O_8$ produced via solid-state synthesis.

2. Materials and Methods
2.1. Samples Preparation

Sodium–vanadium oxide $NaV_3O_8$ was obtained by solid-state method. NH$_4$VO$_3$ (analytical grade) and Na$_2$CO$_3$ (reagent grade) were used as the starting components. The required amounts of the starting materials were weighed within ±0.0001 g (FX40-CJ analytical balance, Japan) and mixed together by grinding in a jasper mortar, then the mixture was heated in an alundum crucible. The temperature for the final stage of sintering was chosen on the basis of DSC and TG data. Thermal analysis was performed using STA 449 F1 Jupiter instrument (NETZSCH, Selb, Germany) in alundum crucibles across a 35–580 °C temperature range at the heating rate of 10 °C/min. Measuring cell was blownthrow with air at arate of 20 mL/min. The data obtained were processed by means
of NETZSCH Proteus software. At first, based on analysis of DSC and TG curves, we made a suggestion on the chemical reactions sequence at the starting mixture heating and temperature at which stabilization of the mass is observed was determined (539 °C). This was chosen as a minimal temperature of synthesis. Temperature increase increases rate of phase formation but on the other hand it can affect adversely on microstructure of material. For that reason we conducted a number of isothermal heat treatments at different temperatures in 4–5 h with following X-ray analysis. Based on the results obtained, optimal temperature and time of sintering were chosen.

2.2. Samples Characterization

The phase composition of the samples was monitored by X-ray diffraction analysis (XRD) on a Rigaku DMAX-2200 diffractometer (Rigaku, Tokyo, Japan) in filtered Cu Kα-radiation generated at 40 kW, 30 mA (λ = 1.54178 Å) in the range of 2θ = 15–70° stepwise with 0.3 s counting time and the step of 0.02°. Jade 6.5. Software was used to calculate unit cell parameters. The error of the cell parameters determining did not exceed 0.02%. The Raman spectra were collected using U-1000 microscope-spectrometer (RENISHAW, Stonehouse, UK) (Ar⁺-radiation, λ = 514 nm) at 100–1200 cm⁻¹.

The morphology of the synthesized material as well as the distribution and shape of its particles were studied using data of scanning electron microscopy (SEM) (MIRA 3 LMU TESCAN, Brno, Czech Republic). The particle-size distribution of the samples was studied using a particle-size analyzer Analysette 22 Nano Tec plus (Fritsch, Selb, Germany).

The ratio V⁴⁺/V⁵⁺ in NaV₃O₈ was determined by X-ray photoelectron spectroscopy (XPS). XPS spectra were collected using a Thermo Fisher Scientific X-ray photoelectron spectrometer (Thermo Scientific, Stonehouse, UK) with monochromatic Al-Kα radiation (hv = 1486 eV). The analyzed area diameter was 400 µm and the binding energy scale was corrected using C1s peak (284.8 eV).

2.3. Measurement of Conductivity

The conductivity of NaV₃O₈ was measured on sintered pellets 10 mm in diameter and 1–2 mm thick. The synthesized NaV₃O₈ powder with particles less than 50 µm in size was pressed in a stainless-steel die at 200–300 MPa and then sintered for 4–5 h at 400 °C in air. Ga-Ag paste applied on the opposite sides of the pellet was used as electrodes. The total conductivity of sample was determined using P-40X potentiostat-galvanostat (Elins, Chernogolovka, Russia) with AC measurements by means of impedance spectroscopy and with DC measurements by pulse potentiometry with time resolution of 2 µs followed by the extrapolation of polarization curves to the pulse time. In addition, the electronic component of conductivity was found using DC with blocking Au electrodes at 20–40 mV. The experiment was performed in the heating and cooling mode in several parallel measurements. The heating/cooling rate was 2 °C/min. The temperature experiment was determined by a platinum–platinum–rhodium thermocouple to an accuracy of ±0.5 °C. Isothermal extracts were made at each temperature. The results obtained at cooling/heating were in good agreement.

3. Results and Discussion

3.1. Synthesis of Sodium–Vanadium Oxide NaV₃O₈

The conditions of synthesis were chosen based on the data of thermal analysis. Figure 1 contains DSC and TG curves for the starting mixture of NH₄VO₃ and Na₂CO₃. There are three peaks on the DSC curve in 200–300 °C temperature region. These peaks correspond to endothermic effects and a change of mass is observed on the TG curve at the corresponding temperatures. The first peak (~196 °C) is related to the start of thermal decomposition of NH₄VO₃. The change of mass that accompanies this process (9.54%) is in good agreement
with the value (9.68%) calculated for the reaction describing the transformation of NH$_4$VO$_3$ into (NH$_4$)$_2$V$_4$O$_{11}$ according to (1).

$$4\text{NH}_4\text{VO}_3 \rightarrow (\text{NH}_4)_2\text{V}_4\text{O}_{11} + 2\text{NH}_3 + \text{H}_2\text{O} \quad (1)$$

Figure 1. DSC and TG curves for the starting mixture of Na$_2$CO$_3$ and NH$_4$VO$_3$ (solid-state synthesis).

The second peak corresponds to the further decomposition of (NH$_4$)$_2$V$_4$O$_{11}$ accompanied by the formation of ammonium polyvanadates, and the third one can be assigned to the decomposition of the latter with the formation of V$_2$O$_5$ [22]. Total mass loss at 350 °C determined from Figure 1 (17.5%) is close to the one calculated based on the total decomposition of NH$_4$VO$_3$ (19.3%). Above ~460 °C the mass of the reaction mixture again begins to decrease slowly, which is related to the release of CO$_2$ after the interaction between Na$_2$CO$_3$ and V$_2$O$_5$, and at 539 °C the mass stabilizes (Figure 1, insert). The mass loss in the region of 460–540 °C was 5.85%, which is close to the one calculated according to the reaction (2), i.e., 6.77%.

$$\text{Na}_2\text{CO}_3 + 3\text{V}_2\text{O}_5 \rightarrow 2\text{NaV}_3\text{O}_8 + \text{CO}_2 \uparrow \quad (2)$$

In the case of the solid solution synthesis [21], the interaction of Na$_2$CO$_3$ and NH$_4$VO$_3$ took place primarily in the solution, and the thermogravimetric analysis of the reaction mixture obtained after the liquid was evaporated demonstrated that the mass stabilizes at ~350 °C, which allowed us to perform the synthesis at 380 °C. The temperature of solid-state synthesis should apparently lie between the temperature of mass stabilization (539 °C) and the temperature of incongruent melting of NaV$_3$O$_8$ (579 °C [23]). Therefore, the temperature of 565 °C was chosen for the synthesis of NaV$_3$O$_8$. The reaction mixture was cooled after 4–5 h and XRD analysis was carried out to monitor the phase composition during isothermal soaking. It was established that at 565 °C the interaction takes 10–12 h to complete. Based on these results, the temperature of 565 °C and the heat treatment time of 12 h were chosen as the optimum conditions for NaV$_3$O$_8$ synthesis.

The results of thermal analysis for NaV$_3$O$_8$ produced under such conditions are shown in Figure 2. One can see that the DSC curve contains one endothermic peak at 579 °C, which corresponds to the incongruent melting [23]. No thermal effects and mass changes have been recorded at lower temperatures. Thus, between the ambient temperature and the temperature of melting, the material obtained is thermally stable.
Intensity (a.u.)

Figure 2. DSC and TG curves for NaV$_3$O$_8$.

3.2. Phase Composition and Microstructure of NaV$_3$O$_8$

The XRD powder pattern for the material obtained through solid-state synthesis is given in Figure 3a1. One can see that most reflections correspond to NaV$_3$O$_8$ phase, PDF2, 28-1171 (Figure 3a2), monoclinic structure, space group P21/m (11). Cell parameters $a = 12.464(1)$ Å, $b = 3.6098(5)$ Å, $c = 7.3451(9)$ Å, $\alpha = \gamma = 90^\circ$, $\beta = 107.36(6)^\circ$ are in good agreement with the literature data [24]. In addition, the pattern contains some reflections of a lower intensity (<2%) indicated by an asterisk in Figure 3a1, which correspond to NaV$_6$O$_{15}$ PDF2, 24-1155 (Figure 3a3). The presence of this phase was previously reported in a number of other works discussing the synthesis of NaV$_3$O$_8$ [13,14]. NaV$_6$O$_{15}$ is also an electrochemically active component [25], but the authors [13,14] point out that the presence of small amounts of NaV$_6$O$_{15}$ alongside NaV$_3$O$_8$ has no effect on the electrochemical properties of the main phase.

![XRD pattern of NaV$_3$O$_8$](image)

Figure 3. (a) XRD pattern of NaV$_3$O$_8$ (1) and line diagrams of powder pattern for NaV$_3$O$_8$ (PDF2, N° 28-1178) (2) and NaV$_6$O$_{15}$ (PDF2, N° 24-1155) (3); (b) Raman spectrum for NaV$_3$O$_8$.

The Raman spectrum for the synthesized sample (Figure 3b) is in good agreement with the literature data for NaV$_3$O$_8$. The characteristic bands observed at 993, 972, 795, 545, 478, 301, 227, 163, 134 cm$^{-1}$ (marked by dotted lines in Figure 3b) practically coincide in their position and intensity with the ones given for NaV$_3$O$_8$ in [26]. According to the literature data, NaV$_3$O$_8$ and LiV$_3$O$_8$ are isostructural [23]. This lets us interpret that the bands in the Raman spectrum for the synthesized sample based on [26] and [27] were Raman spectra for LiV$_3$O$_8$ analyzed. As a result, one can conclude that the low-frequency bands (993 and 972 cm$^{-1}$) correspond to the deformation vibrations, while the medium- and...
high-frequency bands indicate both the deformation vibrations of O-V-O, V-O-V groups, and the stretch vibrations of V-O bonds.

The microstructure of the sodium–vanadium oxide sample produced by solid-state synthesis is shown in Figure 4. The SEM image (Figure 4a,b) and particle size distribution in NaV$_3$O$_8$ samples (Figure 4c) shows that the grain size of the synthesized powder is 1–10 µm. The authors [16] synthesized NaV$_3$O$_8$ by sintering the mixture of Na$_2$CO$_3$ and V$_2$O$_5$ at 400, 500 and 600 °C for 12 h and report that synthesis at the lowest temperature (400 °C) yields the product with the smallest grain size (1–7 µm) characterized by fast intercalation/deintercalation of sodium cations. However, we obtained a powder with practically the same grain size at 565 °C (Figure 4). On the other hand, NaV$_3$O$_8$ produced via aqueous solution followed by heat treatment under conditions similar to the ones applied in [16] (380 °C, 12 h.) had grain size of about 100 nm [21]. Thus, prior interaction of Na$_2$CO$_3$ and NH$_4$VO$_3$ in an aqueous solution affects the grain size of NaV$_3$O$_8$ more than the final heat treatment temperature does.

![Figure 4](image_url)

**Figure 4.** SEM image of NaV$_3$O$_8$ sample with different resolutions, (a) 500x and (b) 20.3kx; (c) particle size distribution in NaV$_3$O$_8$ samples obtained by solid state (c).
3.3. Determining the Content of V$^{4+}$ Ions in the Synthesized NaV$_3$O$_8$: Conductivity Measurement

Successful application of a compound as active cathode material in a power source also depends on its electronic conductivity, which, in the case of oxide vanadium compounds, is determined by the ratio of V$^{4+}$ and V$^{5+}$ [28]. In view of this, investigating the influence of NaV$_3$O$_8$ synthesis technique on V$^{4+}$/V$^{5+}$ ratio is, no doubt, of some interest. The presence and amount of V$^{4+}$ in the material synthesized was determined using XPS. The survey XPS spectrum for NaV$_3$O$_8$ (Figure 5a) was typical for this compound [29]. The spectrum contains clearly identifiable peaks of Na 1s at 1070 eV, C 1s at 285 eV, V 2p at 517 eV, O 1s at 530 eV (Figure 5a).

The high-resolution XPS spectrum for V 2p (Figure 5b) contains clearly identifiable peaks at 517.15 and 524.48 eV, which can be ascribed to the spin-orbit splitting of V$^{5+}$ 2p$^{3/2}$ and V$^{5+}$ 2p$^{1/2}$, respectively [30]. Besides, there are peaks at 515.63 eV (V$^{5+}$ 2p$^{3/2}$) and 523.13 eV (V$^{4+}$ 2p$^{1/2}$) assigned to V$^{4+}$. The content of V$^{4+}$ and V$^{5+}$, calculated from the areas of the peaks, was found to be 8% and 92%, respectively. Synthesis of NaV$_3$O$_8$ via aqueous solution yielded the values of 7% and 93% for V$^{4+}$ and V$^{5+}$, respectively [21]. A slightly higher content of V$^{4+}$ in the case of solid-state synthesis may be related to partial reduction of V$^{5+}$ to V$^{4+}$ by the ammonia released during thermal decomposition of NH$_4$VO$_3$ [22].

The electrical conductivity for NaV$_3$O$_8$ was determined using DC and AC conductivity measurements. The impedance spectroscopy measurements showed that the conductivity of the NaV$_3$O$_8$ samples obtained by solid state does not depend on the frequency. The total conductivity of polycrystalline NaV$_3$O$_8$ sample according to AC impedance spectroscopy measurements practically coincided with the value of conductivity yielded by DC measurements with blocking electrodes, which indicates that across the investigated temperature range, NaV$_3$O$_8$ is a chiefly electronic conductor. In addition, the electrochemical cell of the Ga-Ag│NaV$_3$O$_8$│Ga-Ag was studied by pulse potentiometry in order to determine the electrical resistance of the NaV$_3$O$_8$ sample. First, according to the voltage curves from the current, the maximum permissible load current for this experiment was determined, which was 10 mA. The measurement was performed in two pairs of pulses, +10 mA and −10 mA, with a reference value of 0 mA. The duration of each pulse was 20 μs. The resistance was calculated from the first points of each pulse. In Figure 6a,b is given experimental curves recorded at 25 °C. Pulse potentiometry measurements of conductivity resulted in the value similar to the one obtained by the two above-described methods. Thus, the results of the three measurement techniques practically coincide. Therefore, conductivity of NaV$_3$O$_8$ obeys the Arrhenius equation (Figure 6c) and the activation energy for the sample produced via solid-state synthesis is 13 kJ/mol.
Thus, the results of the three measurement techniques practically coincide. Therefore, conductivity of NaV$_3$O$_8$ obeys the Arrhenius equation (Figure 6c) and the activation energy for the sample produced via solid-state synthesis is 13 kJ/mol.

The conductivity at room temperature was found to be $6.3 \times 10^{-2}$ S cm$^{-1}$. This value is slightly higher than in the case of the sample obtained by aqueous solution technique ($3.2 \times 10^{-2}$ S cm$^{-1}$ [21]), which correlates with the higher content of V$^{4+}$. Similar results were observed in the experiments with LiV$_3$O$_8$ [31]. The conductivity of the LiV$_3$O$_8$ sample synthesized via solid-state reaction was $7.9 \times 10^{-2}$ S cm$^{-1}$ at 20 °C, the value for the sample produced via the method of aqueous solution was $2.5 \times 10^{-2}$ S cm$^{-1}$ (V$^{4+}$ content is 5% and 3%, respectively). Data on the physico-chemical properties of the sample NaV$_3$O$_8$ produced by solid-state synthesis obtained in this work and sample NaV$_3$O$_8$ produced by aqueous solution technique [21] compared to similar sample LiV$_3$O$_8$ [31] are shown in Table 1. Generally, however, the conductivity values for LiV$_3$O$_8$ and NaV$_3$O$_8$ are quite close.

According to the literature data, LiV$_3$O$_8$ and NaV$_3$O$_8$ are isostructural and the only difference between them is the size of the interlayer spacing between vanadium–oxygen layers, where alkali cations are located [32,33]. The largeness of this space affects the mobility of alkali ions, while electronic conductivity is determined by vanadium–oxygen layers, whose structure is the same in both vanadates. Thus, it is reasonable to expect that if the ratios of V$^{4+}$ and V$^{5+}$ for LiV$_3$O$_8$ and NaV$_3$O$_8$ are close, the two compounds will have close values of electronic conductivity, which is the case.

Figure 6. Results of measuring the resistance of the Ga-Ag | NaV$_3$O$_8$ | Ga-Ag cell by pulsepotentiometry. (a) Current pulse, (b) voltage response; t = 25 °C. (c) Temperature dependences of conductivity for NaV$_3$O$_8$ obtained by solid-state synthesis.
Table 1. Data on the physico-chemical properties of the sample NaV$_3$O$_8$ produced by solid-state synthesis obtained in this work and sample NaV$_3$O$_8$ produced by aqueous solution technique [21] compared to similar sample LiV$_3$O$_8$ [31].

| Physico-Chemical Properties | NaV$_3$O$_8$ Solid-State Synthesis | NaV$_3$O$_8$ Aqueous Solution Technique [21] | LiV$_3$O$_8$ Solid-State Synthesis [31] | LiV$_3$O$_8$ Aqueous Solution Technique [31] |
|-----------------------------|------------------------------------|--------------------------------------------|--------------------------------------|--------------------------------------------|
| particle size               | 1–10 µm                            | 100 nm                                     | 1–10 µm                              | 200 nm                                     |
| conductivity, S × cm$^{-1}$ | $6.3 \times 10^{-2}$               | $3.2 \times 10^{-2}$                      | $7.9 \times 10^{-2}$                 | $2.5 \times 10^{-2}$                      |
| V$^{4+}$ content, %         | 8                                  | 7                                          | 5                                    | 3                                          |

4. Conclusions

Sodium–vanadium oxide NaV$_3$O$_8$, which is an attractive cathode material for SIBs, was synthesized via solid-state reaction between NH$_4$VO$_3$ and Na$_2$CO$_3$ at 565 °C. The product was characterized by XRD, thermal analysis and Raman spectroscopy. The morphology, shape and size of its particles and the ratio of V$^{4+}$ and V$^{5+}$ were studied, and AC and DC conductivity measurements were performed. The results were compared with the characteristics of the material having the same composition but produced by the reaction of NH$_4$VO$_3$ and Na$_2$CO$_3$ in a water solution followed by evaporation and heat treatment at 380 °C (aqueous solution method).

The material obtained through solid-state reaction contains a small amount of NaV$_6$O$_{15}$ alongside the monoclinic phase of NaV$_3$O$_8$. The vanadate is thermally stable between the ambient temperature and the temperature of melting; consequently, it can be used in appliances operating at elevated temperatures. It also has a high electronic conductivity ($6.3 \times 10^{-2}$ S × cm$^{-1}$ at room temperature). The high electronic conductivity is an advantage if the vanadate under discussion is proposed as a cathode material for sodium power sources. The conductivity of NaV$_3$O$_8$ synthesized by the method of aqueous solution is twice smaller, thus, at first sight, the vanadate produced in this way is an inferior material compared to its counterpart produced by solid-state reaction. However, the conductivity of NaV$_3$O$_8$ altogether is not very high, and in cathodes of actual power sources it should apparently be combined with another species, characterized by a higher conductivity, e.g., carbon (acetylene black), which is usually used for this purpose. In this case, the difference in the conductivity of the materials obtained via solid-state synthesis and the method of aqueous solution is not important, while the particle size becomes essential. The solid-state technique yields the product with the grain size of 1–3 µm, while using the method of aqueous solution one can obtain a homogeneous nanostructured material with the average grain size of nearly 100 nm. According to the literature data, nanostructured cathode materials considerably improve the kinetics of alkali cations intercalation/deintercalation, and increase the capacity of power sources and their cyclability and coulombic efficiency. Therefore, the method of aqueous solution is a better alternative for the production of NaV$_3$O$_8$ compared to the solid-state technique.

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