THE NEUTRON STAR CENSUS

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ABSTRACT

The paucity of old isolated accreting neutron stars in ROSAT observations is used to derive a lower limit on the mean velocity of neutron stars at birth. The secular evolution of the population is simulated following the paths of a statistical sample of stars for different values of the initial kick velocity, drawn from an isotropic Gaussian distribution with mean velocity $0 \leq \langle V \rangle \leq 550$ km s$^{-1}$. The spin-down, induced by dipole losses and by the interaction with the ambient medium, is tracked together with the dynamical evolution in the Galactic potential, allowing for the determination of the fraction of stars which are, at present, in each of the four possible stages: ejector, proppeller, accretor, and georotator. Taking from the ROSAT All Sky Survey an upper limit of $\sim 10$ accreting neutron stars within $\sim 140$ pc from the Sun, we infer a lower bound for the mean kick velocity, $\langle V \rangle \simeq 200$–300 km s$^{-1}$, corresponding to a velocity dispersion $\sigma_v \gtrsim 125$–190 km s$^{-1}$. The same conclusion is reached for both a constant magnetic field ($B \sim 10^{12}$ G) and a magnetic field decaying exponentially with a timescale $\sim 10^3$ yr. Such high velocities are consistent with those derived from radio pulsar observations. Present results, moreover, constrain the fraction of low-velocity stars, which could have escaped pulsar statistics, to less than 1%.

Subject headings: accretion, accretion disks — stars: kinematics — stars: magnetic fields — stars: neutron — stars: statistics — X-rays: stars

1. INTRODUCTION

Isolated neutron stars (NSs) are expected to be as many as $10^8$–$10^9$, $\sim 1\%$ of the total stellar content of the Galaxy. Young NSs, active as pulsars, comprise only a tiny fraction ($\sim 10^{-3}$–$10^{-4}$) of the entire population, and about 1000 have been detected in radio surveys. It is thus an observational fact that most of the NSs remain undetected as yet. Despite intensive searches at all wavelengths, only a few putative isolated NSs which are not radio pulsars (or soft $\gamma$ repeaters) have been recently discovered in the X-rays with ROSAT (Walter, Wolk, & Neuhäuser 1996; Haberl et al. 1996; Haberl, Motch, & Pietsch 1998; Schwöpe et al. 1999; Motch et al. 1999). All these sources emit a thermal spectrum at $\sim 100$ eV, and the derived column densities place them at relatively close distances (at most a few hundred parsecs) implying luminosities not in excess of $10^{32}$ ergs s$^{-1}$. For RX J1856–3754, an extremely faint optical counterpart ($m_V \sim 26$) have been firmly established by now (Walter & Matthews 1997) while a possible counterpart has been found in the X-ray error box of RX J0720–3125 by Kulkarni & van Kerkwijk 1998 (see also Motch & Haberl 1998). For the other remaining candidates, plate searches have only placed limits down to $m_V \gtrsim 24$.

Although the extreme X-ray to optical flux ratio ($>10^3$) makes the NS option rather robust, the exact nature of their emission is still controversial. Up to now, two main possibilities have been suggested, either relatively young NSs radiating away their residual internal energy or much aged NSs accreting the interstellar gas. Unmagnetized, cooling models can reproduce the full spectral energy distribution (SED), including the optical excess observed in the best studied object RX J1856–3754, if the surface temperature depends on the latitude or for Fe/Si-ash atmospheres (Walter & Matthews 1997; Walter & An 1998; note, however, that spectra computed by Pavlov et al. 1996 for similar compositions fail to reproduce the observed SED). Accreting, pure H, atmospheres around nonmagnetic NSs produce a hard X-ray tail (Zampieri et al. 1995) that is not observed in these sources. However, as in cooling models, the hardening decreases for increasing $B$ and the essential features of the SED may have a quite natural explanation in terms of magnetized, H, accretion models (Zane, Turolla, & Treves 1999).

Cooling NSs have short lifetimes ($\sim 10^6$ yr; Page 1998) and thus might be relatively rare objects. On the other hand, at least if the Bondi-Hoyle scenario applies, accretion can be severely reduced when the NS velocity (relative to the interstellar medium) exceeds 40 km s$^{-1}$ so the process of accretion itself might be unable to produce the typical luminosities inferred from ROSAT data. When available, proper motion measurements for some of the five isolated NS candidates detected so far will prove decisive in assessing the true nature of these sources. Meanwhile, we feel that a more thorough analysis of the statistical properties of NSs is of interest and can be useful in providing indirect evidence in favor of or against the accretion scenario.

As discussed by Lipunov (1992), isolated NSs can be classified into four main types: ejectors, propellers, accretors, and georotators. In ejectors the relativistic outflowing momentum flux is always larger than the ram pressure of the surrounding material so they never accrete and are either active radio pulsars or dead pulsars, spun down by dipole losses. In propellers the incoming matter can penetrate down to the Alfvén radius but not further because of the centrifugal barrier, and, although stationary inflow cannot occur, the piling up of the material at the Alfvén radius may give rise to (supposedly short) episodes of accretion.

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(Treves, Colpi, & Lipunov 1993; Popov 1994). Steady accretion is also impossible in georotators where (similarly to the Earth) the Alfven radius exceeds the accretion radius, so that magnetic pressure dominates everywhere over the gravitational pull. It is the combination of the star period, magnetic field, velocity, and ambient medium that decides which type a given isolated NS belongs to, and, since both \( P, B, V, \) and \( n \) change during the star evolution, a NS can go through different stages in its lifetime. This argument shows that, at variance with what was assumed in earlier investigations (Treves & Colpi 1991; Blaes & Madau 1993; Zane et al. 1995) stationary accretion onto an isolated old NS (ONS) is a particular, we explore the effects induced on the current census of NSs by varying the mean value of the kick velocity. In earlier investigations (Treves & Colpi 1991; Blaes & Madau 1993; Madau & Blaes 1994; Zane et al. 1995) who modeled the present velocity distribution, one of the key parameters governing accretion. Until now, however, little attention was paid to the NSs magnetorotational evolution. Only recently, this issue was discussed in some detail by Livio, Xu, & Frank (1998) and Colpi el al. (1998), who found that, for a given velocity distribution, the number of accreting sources depends strongly on the way the magnetic field decays.

Goal of this investigation is to consider these two issues simultaneously, coupling the dynamical and the magnetorotational evolution for the isolated NS population. In particular, we explore the effects induced on the current census of NSs varying the mean value of the kick velocity. In earlier investigations (Treves & Colpi 1991; Blaes & Madau 1993; Zane et al. 1995) who modeled the present velocity distribution, one of the key parameters governing accretion. Until now, however, little attention was paid to the NSs magnetorotational evolution. Only recently, this issue was discussed in some detail by Livio, Xu, & Frank (1998) and Colpi el al. (1998), who found that, for a given velocity distribution, the number of accreting sources depends strongly on the way the magnetic field decays.

The dynamical evolution of NSs in the Galactic potential was studied by several authors (Paczynski 1990; Blaes & Rajagopal 1991; Blaes & Madau 1993; Madau & Blaes 1994; Zane et al. 1995) who modeled the present velocity distribution, one of the key parameters governing accretion. Until now, however, little attention was paid to the NSs magnetorotational evolution. Only recently, this issue was discussed in some detail by Livio, Xu, & Frank (1998) and Colpi et al. (1998), who found that, for a given velocity distribution, the number of accreting sources depends strongly on the way the magnetic field decays.

2. THE MODEL

In this section we summarize the main hypothesis introduced to describe the evolution of single stars and outline shortly the technique used to explore their statistical properties, referring to Popov & Prokhorov (1998, 1999a, 1999b) for details on spatial evolution calculations.

2.1. Dynamical Evolution

The dynamical evolution of each single star in the Galactic potential is followed solving its equations of motion. The potential, proposed by Miyamoto & Nagai (1975) and adopted later by Paczynski (1990), is given by the superposition of a spherical halo and of two flattened bulge/disk components. In Galactocentric cylindrical coordinates \( R, Z, r = (R^2 + Z^2)^{1/2} \), they are expressed as

\[
\Phi_H(R, Z) = - \frac{GM_c}{r_c} \left[ \frac{1}{2} \ln \left( 1 + \frac{r^2}{r_c^2} \right) + \frac{r_c}{r} \tan^{-1} \left( \frac{r}{r_c} \right) \right],
\]

and

\[
\Phi_i(R, Z) = - \frac{GM_i}{\sqrt{R^2 + \left[ a_i + (Z^2 + b_i^2)^{1/2} \right]^2}},
\]

where the index \( i \) stands both for \( B \) (bulge) and \( D \) (disk), and \( H \) stands for halo. The values of the parameters appearing in equations (1) and (2) are summarized in Table 1.

In their motion through the Galaxy, NSs interact with the interstellar medium (ISM) when (and if) they enter the propeller or the accretor phase. In these two stages the accreting material affects significantly the star spin because braking torques arise (see §2.3). Since the period evolution depends on both the star velocity and the local density of the interstellar medium, any attempt to investigate the statistical properties of the NS population should incorporate a (detailed) model of the distribution of the ISM. Unfortunately, the distribution of molecular and atomic hydrogen in the Galaxy is highly inhomogeneous and only an averaged description is possible. Here we use the analytical distributions from Bochkarev (1992) and Zane et al. (1995). Denoting with \( n_{H_1} \) and \( n_{H_2} \) the neutral and molecular hydrogen number density, the total proton density is given by

\[
n(R, Z) = n_{H_1} + 2n_{H_2}.
\]

The molecular hydrogen distribution is approximated as

\[
n_{H_2}(R, Z) = n_2(R) \exp \left[ - \frac{Z^2}{2(70 \ \text{pc}^2)} \right],
\]

where \( n_2(R) \) is tabulated in Bochkarev (1992). The map of atomic hydrogen is more complex and for \( R \leq 3.4 \ \text{kpc} \) we assume

\[
n_{H_1} = n_\alpha(R) \exp \left[ - \frac{Z^2}{2(140 \ \text{pc}^2)} \left( \frac{R}{2 \ \text{kpc}} \right)^2 \right].
\]

The preceding expression becomes inaccurate inside \( \sim 1 \ \text{kpc} \), where the gas distribution is dominated by a rotating ring and dense clouds. However, since we do not calculate the evolution of NSs born in the central 2 kpc, this is not going to be of any relevance (see Zane, Turolla, & Treves

| Parameter | Halo | Bulge | Disk |
|-----------|------|-------|------|
| \( r \) (kpc) | 6.0  | ...   | ...  |
| \( a \) (kpc) | ...  | 0.0   | 3.7  |
| \( b \) (pc)  | ...  | 277   | 200  |
| \( M (M_\odot) \) | \( 5.0 \times 10^{10} \) | \( 1.1 \times 10^{10} \) | \( 8.1 \times 10^{10} \) |
The density of cold and warm H I at $3.4 \text{kpc} \leq R \leq 8.5 \text{kpc}$ can be fitted by

$$n_{\text{HI}} = 0.345 \exp \left[ -\frac{Z^2}{2(212 \text{ pc})^2} \right] + 0.107 \exp \left[ -\frac{Z^2}{2(530 \text{ pc})^2} \right] + 0.064 \exp \left[ -\frac{Z}{403 \text{ pc}} \right],$$

while at radii larger than 8.5 kpc we use

$$n_{\text{HI}} = n_0(R) \exp \left[ -\frac{Z^2}{2(530 \text{ pc})^2} \left( \frac{R}{8.5 \text{ kpc}} \right)^2 \right],$$

where $n_0(R)$ and $n_0$ are again taken from Bochkarev (1992). The total hydrogen density distribution used in our computations is shown in Figure 1; the density in the galactic plane varies by more than 1 order of magnitude, ranging from 0.1 to 4.3 cm$^{-3}$. Within a region of $\sim 140$ pc around the Sun, the ISM is underdense, and we take $n = 0.07$ cm$^{-3}$ (see Zane et al. 1996b).

In our model we assume that the NS birthrate is constant in time and proportional in magnitude to the square of the local gas density (see, e.g., Cox 1983; Firmani & Tutukov 1994). This implies that NSs are preferentially produced in the molecular ring region and migrate through the Galaxy during their evolution, due to the large kick velocities acquired at birth. Stars are assumed to be born in the Galactic plane ($Z = 0$) and in the range $2 \text{kpc} < R < 16 \text{kpc}$; this limitation has no major influence on the results, and on the number of sources found in the solar vicinity in particular. In the present investigation all effects of NSs born in binary systems (see, e.g., Iben & Tutukov 1998) have been neglected. Mirroring the birthrate of massive stars, also the NS rate was likely to be higher in past (White & Ghosh 1998), so that our assumption of a constant NS birthrate is just a simplification. The effect of a time-dependent NS formation rate will deserve further study.

Neutron stars at birth have a circular velocity determined by the Galactic potential. Superposed to this ordered motion a kick velocity $V$ is imparted in a random direction. The exact form of the kick distribution is still uncertain (see, e.g., Lipunov, Postnov, & Prokhorov 1996a; Iben & Tutukov 1998; Belczynski & Bulik 1999). Here we use an isotropic Gaussian distribution with zero mean velocity vector relative to the local circular speed, and one-dimensional velocity dispersion $\sigma_V$, simply as a mean to model the true pulsar distribution at birth (see, e.g., Cordes 1998). The resulting distribution for the modulus $V$ is characterized by a mean velocity $\langle V \rangle \equiv (8/\pi)^{1/2} \sigma_V$, which is varied in the interval 0–550 km s$^{-1}$. The velocity dispersion of the NS progenitors, $\sim 20$ km s$^{-1}$, has been neglected and runs with $\langle V \rangle$ of this order mimic a NSs population with zero mean kick velocity at birth.

For each star the dynamical evolution has been followed up to present time. The evolution of the spin period $P$ (as described in § 2.3) is also computed, keeping memory of the different phases the neutron star experiences (ejector, propeller, etc.). A number of representative evolutionary paths have been calculated, placing the stars at a given location in the galactic plane, with a randomly oriented kick drawn from the specified Gaussian distribution. Each evolutionary track is statistically independent and gives a unique galactic orbit together with a unique history. Each orbit is recorded every time the star crosses the boundary between two adjacent spatial cells in which the Galaxy is divided. The time of transition between two phases is also recorded and stored. Approximately, a star takes $10^6$ yr to cross a cell, which means that the star position (and status) is recorded $\sim 10^4$ times in a total orbital time of $10^{10}$ yr. To mimic continuous star formation a single track is repeatedly used shifting the time ahead. In addition, tracks born in denser regions of the galactic plane, where the rate of star formation is higher, acquire, accordingly, a higher statistical weight. One orbit integration samples the behavior of nearly $10^6$ stars born with the same initial conditions at different times. (We refer for details to the “Scenario Machine” of Lipunov, Postnov, & Prokhorov 1996b.) A number of independent runs have been performed using different number of objects, up to a maximum of $\sim 10^4$ so giving $\sim 10^5$ stellar paths. The runs have been carried out using different seeds for the random orientation of kicks. Statistical fluctuations on the number of stars in each stage are typically of a few percent.
2.2.  Accretion Physics

The accretion rate was calculated according to the Bondi formula

$$M = \frac{2\pi (GM)^2 m_p n(R, Z)}{(V^2 + V_c^2)^{3/2}} \approx 10^{11} n v_{10}^{-3} \text{ g s}^{-1} ,$$  

(8)

where $m_p$ is proton mass, the sound speed $V_c$ is always 10 km s$^{-1}$, and $v_{10} = (V^2 + V_c^2)^{1/2}$ in units of 10 km s$^{-1}$. Here and in the following $M$ and $R$ denote the NS mass and radius, which we take equal to 1.4 $M_\odot$ and 10 km, respectively, for all stars. Assuming, for the sake of simplicity, a nonrelativistic efficiency $\sim GM/Rc^2$, the accretion luminosity is given by

$$L = \frac{GM^2}{R} .$$  

(9)

Although the spectrum emitted by accreting NSs may differ rather substantially from a blackbody at the star effective temperature (see Zampieri et al. 1995 for low-field spectra and Zane et al. 1999 for magnetized models) here we assume pure thermal emission. Even in this simplified case, the effective temperature depends on the star dipole field because accretion occurs only at the two polar caps of radius $R_{cap} = (R/R_\lambda)^{1/2}$,

$$R_{cap} = 9.5 \times 10^{3} \mu_{30}^{-2/7} n^{1/7} v_{10}^{-3/7} \text{ cm} ;$$  

(10)

where $R_\lambda \approx 1.1 \times 10^{10} n^{-2/7} v_{10}^{6/7} \mu_{30}^{3/7}$ cm is the Alfven radius and $\mu_{30}$ is the star magnetic dipole moment in units of 10$^{30}$ G cm$^3$ (see, e.g., Zane et al. 1996b; Konenkov & Popov 1997). The reduced emitting area produces harder spectra, with an effective temperature $\sim 3$–4 times larger than in the unmagnetized case

$$T_{\text{eff}} \approx 5 \times 10^8 \mu_{30}^{1/7} n^{3/14} v_{10}^{-3/14} K ;$$  

(11)

typical temperatures are around 100 eV for $V \sim 100$ km s$^{-1}$ for nonevolving magnetic field, and a little bit lower for evolving magnetic fields.

2.3.  Period Evolution

All neutron stars are assumed to be born with a period $P(0) = 0.02$ s, and a magnetic moment either $\mu_{30} = 1$ or $\mu_{30} = 0.5$. Different distributions of the initial periods, like the one recently proposed by Spruit & Phinney (1998), were also tested and produced very similar results.

The ejector regime begins with the pulsar phase and proceeds also after the breakdown of the coherence condition when the star becomes a dead, or silent, pulsar. In this phase the energy losses are due to magnetic dipole radiation, and the period increases in time according to

$$P = P(0) + 3 \times 10^{-4} \mu_{30}^{1/2} t^{1/2} \text{ s} ,$$  

(12)

where $t$ is in yr. When the gravitational energy density of the incoming interstellar gas exceeds the outward momentum flux at the accretion radius, $R_{ac} \approx 2GM/v_c^2$, matter starts to fall in. For this condition to be met, the period must have reached a critical value

$$P_*(E \rightarrow P) \approx 10^9 \mu_{30}^{1/2} n^{-1/4} v_{10}^{-1/2} \text{ s} ,$$  

(13)

which is attained by dipole braking (for a constant field) in a time

$$t_P \approx 10^9 \mu_{30}^{-1} n^{-1/2} v_{10} \text{ yr} .$$  

(14)

When $P > P_*(E \rightarrow P)$ matter can penetrate down to the Alfven radius, but the interaction with the rotating magnetosphere prevents accretion to go any further because of the centrifugal barrier. The NS is now in the propeller phase, rotational energy is lost to the ISM, and the period keeps increasing at a rate

$$\frac{dP}{dt} \approx \frac{MR^2}{I} P \approx K P^a \text{ s}^{-1} .$$  

(15)

Here we take $K = 2.4 \times 10^{-14} \mu_{30}^{8/7} n^{-3/7} v_{10}^{-9/7}$, $a = 1$ (Shakura 1975) and $I = 10^{45}$ g cm$^2$ is the star moment of inertia.

It should be stressed, however, that our expression for the propeller spin-down is just an approximation. The propeller physics is very complicated and its thorough understanding requires a full two- or even three-dimensional MHD investigation of accretion onto a rotating dipole (see, e.g., Toropin et al. 1999; see also other spin-down formulae for that stage in Lipunov & Popov 1995). The propeller spin-down, as modeled by equation (15), is very efficient and acts on a typical timescale

$$t_P \approx 1.3 \times 10^9 \mu_{30}^{-8/7} n^{-3/7} v_{10}^{-9/7} \text{ yr} .$$  

(16)

Numerical simulations (Toropin et al. 1999; Y. M. Toropin 1999, private communication) seem indeed to confirm that spin-down in the propeller phase is very fast due to the large mass expulsion rate. Note that the present expression for the propeller torque is somewhat different from that adopted by Treves et al. (1993, 1998). As the star moves through the inhomogeneous ISM a transition from the propeller back to the ejector phase may occur if the period attains the critical value

$$P_A(P \rightarrow E) \approx 3 \mu_{30}^{6/7} v_{10}^{8/7} n^{-2/7} \text{ s} .$$  

(17)

Note that the transitions $P \rightarrow E$ and $E \rightarrow P$ are not symmetric because the two periods, equations (13) and (17), derive from the same physical condition but evaluated at different radii, as first discussed by Shvartsman in the early 1970s.

Accretion onto the star surface occurs when the corotation radius $R_0 = (GM/P^2)^{1/3}$ becomes larger than the Alfven radius (and $R_\lambda < R_{ac}$ see below). This implies that braking torques have increased the period up to

$$P_A(P \rightarrow A) \approx 420 \mu_{30}^{8/7} n^{-3/7} v_{10}^{9/7} \text{ s} .$$  

(18)

As soon as the NS enters the accretor phase, torques produced by stochastic angular momentum exchanges in the ISM slow down the star rotation to the equilibrium period

$$P_{eq} = 2.6 \times 10^3 v_{10}^{-2/3} n^{2/3} \mu_{30}^{2/3} v_{10}^{13/3} \text{ s} ,$$  

(19)

where $v_{10}$ the turbulent velocity of the ISM (Lipunov & Popov 1995; Konenkov & Popov 1997).

Actually, the condition that $P \geq P_A$ is not sufficient to guarantee that matter is captured at the accretion radius. At the very low accretion rates expected for fast, isolated NSs, it could be that the Alfven radius is larger than the accretion radius. The condition $R_\lambda < R_{ac}$ translates into a limit for the star velocity

$$v \leq 410 n^{1/10} \mu_{30}^{-1/5} \text{ km s}^{-1} .$$  

(20)

Above this velocity the NS behaves as a georotator and it experiences a torque which is computed in the same way as
Figure 2.—Different stages of old NSs at present as a function of the star velocity and magnetic dipole moment.

in the propeller stage. The star can enter the georotator phase only from the propeller or accretor stage.

Figure 2 illustrates the various possible stages for a NS $10^{10}$ yr old as a function of the star velocity and magnetic field for a constant ambient density of $1 \text{ cm}^{-3}$. The propeller region in Figure 2 is very small, as a consequence of the extremely efficient spin-down implied by equation (15) with our choice of the parameters $a$ and $K$.

3. RESULTS AND DISCUSSION

In this section, we present the results of our numerical simulations both in the cases of a constant and of a decaying magnetic field.

3.1. The NS Census for a Nondecaying Field

Here we consider two values for the magnetic dipole moment ($\mu_{30} = 0.5$ and $\mu_{30} = 1$) as representative of the constant NS magnetic field. The present fraction of NSs in the ejector and accretor stages as a function of the mean kick velocity is shown in Figure 3. Statistical errors are typically $\sim 2\%$. Propellers and georotators are much less abundant and never exceed $\sim 1\%$ of the total number. In addition, their fractions oscillate intrinsically because of the changes in the velocity and in the ISM density along the star trajectory. These effects add further noise to the statistical fluctuations and, given the small number of sources in these two states, prevent any definite conclusion about the dependence of the fractions from the mean kick velocity. We note that the fraction of accretors increases with the field strength, in agreement with the findings of Livio, Xu, & Frank (1998) and Colpi et al. (1998). Highly magnetized NSs suffer, in fact, a more severe spin-down during the ejector and propeller phases and reach the accretion phase earlier in their history. For large enough mean kick velocities ($>400 \text{ km s}^{-1}$ for $\mu_{30} = 1$ and $>300 \text{ km s}^{-1}$ for $\mu_{30} = 0.5$) the fraction of accretors becomes very small and again results become statistically uncertain. We note also that the numerical simulation produces a picture of the present status of the Galactic NS population, which is consistent with that emerging from Figure 2. In fact, if we assume that the velocity gives a measure of the average kick, we see, with reference to $\mu_{30} = 1$, that accretors are more abundant than ejectors up to $\sim 100 \text{ km s}^{-1}$, propellers are extremely rare and georotators nearly absent. This is precisely what Figure 3 shows.

To obtain an estimate of the number of accreting sources in the solar vicinity (taken to be a sphere of radius 140 pc centered on the Sun), we used all the stars contained in a torus of the same radius located at 8 kpc from the center of the Galaxy. The result was then rescaled to the volume of interest and is shown in Figure 4. Here, and in the following the total number of Galactic NSs was assumed to be $10^9$. As expected, the local density is a sensitive function of the kick velocity and varies between $n \sim 8.5 \times 10^{-3} \text{ pc}^{-3}$ and $n \sim 6 \times 10^{-4} \text{ pc}^{-3}$ for $\langle V \rangle = 0$ and 190 km s$^{-1}$, respectively. These figures should be compared with $n \sim 1.4 \times 10^{-3} (N/10^9) \text{ pc}^{-3}$ as derived by Paczyński (1990) for a zero mean velocity and with $n \sim 3-7 \times 10^{-4} (N/10^9)$ found by Blaes & Madau (1993) and Zane et al. (1995) for an initial mean velocity of $\sim 60 \text{ km s}^{-1}$.

The density of isolated NSs projected onto the Galactic plane is $\sim 2.4 \times 10^5 (N/10^9) \text{ kpc}^{-2}$ for average initial velocities $\sim 200 \text{ km s}^{-1}$ and a scale height of 200 pc. This figure is close to the one deduced by Neuhäuser & Trümper (1999) from radio pulsars observations (Lyne et al. 1998) with the assumption of a pulsar lifetime $\sim 10^7$ yr. We would like to

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**Figure 3.**—Fractions of NSs in the different stages vs. the mean kick velocity for $\mu_{30} = 0.5$ (triangles) and $\mu_{30} = 1$ (diamonds); typical statistical uncertainty is $\sim 2\%$. 
note, however, that a projected density \( \sim 10^3 \) kpc\(^{-2} \) is now obtained for \( N = 10^9 \) instead of \( 10^8 \) (as in Madau & Blaes 1994; see also Neuhäuser & Trümper 1999) because of the larger mean velocity at birth. A total number \( \sim 10^8 \) appears to be consistent with the nucleosynthesis and chemical evolution of the Galaxy, while \( 10^8 \) is derived from radio pulsars observations. For the time being, it is still uncertain if all NSs experience an active radio pulsar phase, due to low or unusually high initial magnetic fields or/and long periods (Gotthelf 1998), or to the fall-back in the aftermath of the supernova explosion (Colpi, Shapiro, & Wassermann 1996; Geppert, Page, & Zannias 1999). Radio pulsars are observed only in a fraction of SNRs (see, e.g., Kaspi 1996; Frail 1998), and even some of these coincidences are doubtful, so there is a serious possibility that the total number of NSs derived from radio pulsar statistics is only a lower limit.

In order to compare the expected number of accreting ONs with the ROSAT All Sky Survey (RASS) results, we evaluated the number of those ONs, within 140 pc from the Sun, producing an unabsorbed flux of \( 10^{-13} \) ergs cm\(^{-2} \) s\(^{-1} \) at energies \( \sim 100 \) eV (the contribution from sources at larger distances is found to be negligible). This flux limit should correspond to a RASS count rate of 0.01 counts s\(^{-1} \) for a blackbody spectrum, once the interstellar absorption and the ROSAT response function are accounted for. The results are illustrated in Figure 5 (above 200 km s\(^{-1} \) statistical errors are dominant). As expected, the dependence of the number of visible sources on the kick velocity is rather strong. The main result is that for mean velocities below 200 km s\(^{-1} \) the number of ONs with a flux above the RASS detection limit would exceed 10. Most recent analyses on the number of isolated NSs in the RASS (Neuhäuser & Trümper 1999) indicate that the upper limit is below 10. This implies a lower limit for the mean kick velocity at birth of \( \sim 200 \) km s\(^{-1} \) for a total number of stars \( \sim 10^9 \).

This result is in agreement with the estimates derived from pulsar statistics. An important aspect is that our results exclude the possible presence of a low-velocity tail at birth in excess to that contained in a Gaussian with \( \langle V \rangle \sim 200 \) km s\(^{-1} \), i.e., the 0.05\% [\( \sim (2\pi)^{-3/2}[V/\sigma]^3 \)] of the whole population, when considering stars having \( V < 40 \) km s\(^{-1} \).

3.2. The NS Census for a Decaying Field

The time evolution of the magnetic field in isolated NSs is still a very controversial issue, and no firm conclusion has been established as yet (Bhattacharya et al. 1992). A strong point is that radio pulsar observations (see, e.g., Lyne et al. 1998) seem to rule out fast decay with typical times less than \( \approx 10 \) Myr, but this does not exclude the possibility that \( B \) decays over much longer timescales \( (t_d \sim 10^8-10^{11}) \) yr. For this reason we have investigated to what extent the decay of the \( B \)-field influences the results presented in the previous section. We refer here only to a very simplified picture in which \( B(t) = B(0) \exp (-t/t_d) \), and no attempt is made to justify this law on a physical ground. (See Popov & Prokhorov 1999a, 1999b for a more complete study in the parameter space.) In this respect we just mention that detailed models predict both exponential (quite similar to the one assumed here) and nonexponential decay (e.g., a power law, Urpin & Konenkov 1997). Calculations have been performed for \( t_d = 1.1 \times 10^7 \) yr, \( t_d = 2.2 \times 10^8 \) yr and \( \mu_{30}(0) = 1 \). Since no bottom field was specified, the magnetic moment becomes very low for stars born \( \sim 10^{10} \) yr ago (\( \sim 10^{26} \) and \( \sim 10^{28} \) G cm\(^3 \) for the two values of \( t_d \), respectively).

Results are summarized in Figure 6. As it is expected (see Colpi et al. 1998), the number of propellers is significantly increased with respect to the nondelaying case, while ejectors are now less abundant. Georotators are still very rare, \( \lesssim 1\% \), and are not shown in Figure 6. The fraction of accretors is approximately the same for the two values of \( t_d \) and, at least for low mean velocities, is comparable to that of the nondelaying field while, at larger speeds, it seems to be somehow higher. This shows that the fraction of accretors depends to some extent on how the magnetic field decays. We know that a core field decaying over a time \( \sim 10^8 \) yr...
before freezing would produce an underabundance of accretors relative to the case of a constant field (Colpi et al. 1998) because NSs persist in the ejector or propeller phase never approaching the accretor phase. By contrast, a fast and progressive decay of $B$ would lead to an overabundance of accretors because this situation is similar to "turning off" the magnetic field, i.e., quenching any magnetospheric effect on the infalling matter.

Summarizing, we can conclude that, although both the initial distribution and the subsequent evolution of the magnetic field strongly influence the NS census altering the fraction of ejectors relative to propellers, the lower bound on the average kick derived from ROSAT surveys is not very sensitive to $B$, at least for not too extreme values of $t_d$ and $\mu(0)$, within this model.

4. CONCLUSIONS

In this paper we have investigated how the present distribution of neutron stars in the different stages (ejector, propeller, accretor, and georotator) depends on the star mean velocity at birth. On the basis of a total of $\sim 10^6$ NSs, the fraction of accretors was used to estimate the number of sources within 140 pc from the Sun which should have been detected by ROSAT. Most recent analysis of ROSAT data indicates that no more than $\sim 10$ non–optically identified sources can be accreting ONSs. This implies that the average velocity of the NS population at birth has to exceed $\sim 200 \text{ km s}^{-1}$, a figure that is consistent with that derived from radio pulsars statistics. We have found that this lower limit on the mean kick velocity is substantially the same either for a constant or a decaying $B$ field, unless the decay timescale is shorter than $\sim 10^9$ yr. Since observable accretion-powered ONSs are slow objects, our results exclude also the possibility that the present velocity distribution of NSs is richer in low-velocity objects with respect to a Maxwellian. The paucity of accreting ONSs seem therefore to lend further support in favor of neutron stars as being very fast objects spending most of their lives in the ejector phase.

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