Robust Training of Graph Neural Networks via Noise Governance

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ABSTRACT
Graph Neural Networks (GNNs) have become widely-used models for semi-supervised learning. However, the robustness of GNNs in the presence of label noise remains a largely under-explored problem. In this paper, we consider an important yet challenging scenario where labels on nodes of graphs are not only noisy but also scarce. In this scenario, the performance of GNNs is prone to degrade due to label noise propagation and insufficient learning. To address these issues, we propose a novel RTGNN (Robust Training of Graph Neural Networks via Noise Governance) framework that achieves better robustness by learning to explicitly govern label noise. More specifically, we introduce self-reinforcement and consistency regularization as supplemental supervision. The self-reinforcement supervision is inspired by the memorization effects of deep neural networks and aims to correct noisy labels. Further, the consistency regularization prevents GNNs from overfitting to noisy labels via mimicry loss in both the inter-view and intra-view perspectives. To leverage such supervisions, we divide labels into clean and noisy types, rectify inaccurate labels, and further generate pseudo-labels on unlabeled nodes. Supervision for nodes with different types of labels is then chosen adaptively. This enables sufficient learning from clean labels while limiting the impact of noisy ones. We conduct extensive experiments to evaluate the effectiveness of our RTGNN framework, and the results validate its consistent superior performance over state-of-the-art methods with two types of label noises and various noise rates.

CCS CONCEPTS
• Information systems → Data mining.

KEYWORDS
GNNs; semi-supervised learning; label noise; robustness

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1 INTRODUCTION
In real-world applications, a set of objects and their relationships can often be represented naturally as a graph. The graph data structure is widely employed in various domains such as biology, transportation, and social science. In the past decade, Graph Neural Networks (GNNs) have shown promising capacity in modeling graph data [13, 20, 38]. Typically, GNNs adopt a message passing and aggregation procedure to effectively propagate information via the graph structure. This mechanism makes GNNs very suitable for semi-supervised graph learning (e.g., node classification [1, 32]).

While GNNs are generally effective, most of the existing approaches assume that labels are sufficient and clean. However, in practice, node labels can be both scarce and noisy. For example, consider a graph from social media whose node labels are contributed by users. It is often the case that only a small fraction of users would participate in label generation, and intentionally or for other reasons, some of the labels do not reflect the truth. Another example is crowd-sourcing node labels, e.g., fake news annotation and medical knowledge graph annotation. It is easy to see that the annotation process is labor-intensive and expensive, and almost inevitably, label errors are introduced due to subjective judgment. Such cases will lead to graphs with scarce and noisy node labels. It has already been observed that noisy labels could pose a severe threat to the generalization performance of deep learning models [2, 42]. Therefore, developing label-efficient and noise-resistant GNNs is an important and challenging problem.

In the literature, robust deep learning in the presence of noisy labels has been explored mainly in applications with non-graph data such as images. Several strategies have been developed to combat label noises, e.g., sample selection [14, 16, 24], robust loss
functions [10, 34, 44], and loss correction [27, 29]. However, simply incorporating these approaches into GNNs will be insufficient (we will empirically show this in experiments). We observe that one unique characteristic of this problem with GNNs is that the scarcity of labels causes difficulties for nodes to receive sufficient supervision from labeled neighbors. Meanwhile, nodes in graphs are directly influenced by potential noises through message passing. Failing to balance the two would either lead to massive erroneous supervision from noisy labels or end up with insufficient learning.

Hence, a main challenge to solving this problem is how to effectively leverage supervision of clean labels while limiting the impact of noisy ones. Previous studies mainly focused on leveraging supervision of labels, but neglected how to limit the impact of noisy labels. For example, recently, NRGNN [6] investigated a robust GNN with noisy and sparse labels. It proposed to link unlabeled nodes with labeled nodes and further mine accurate pseudo-labels to provide more supervision. However, NRGNN mainly emphasized leveraging supervision of labels, which mixed up clean and noisy labels in its learning process. Whereas, as explained above, explicitly governing noises (i.e., limiting the impact of noisy labels) is necessary in order to further boost the robustness of GNNs.

To this end, we propose a novel GNN framework called RTGNN (Robust Training of Graph Neural Networks via Noise Governance) that is capable of conducting robust learning with scarce and noisy node labels. As a distinguished design of our model, we develop a fine-grained noise governance strategy in semi-supervised learning. Due to the fact that deep neural networks (DNNs) tend to prioritize learning simple patterns first and may overfit to noises [2], we first propose an effective and scalable loss-based label division method to identify potentially noisy labels. Further, besides the commonly-used label supervision, we introduce self-reinforcement and consistency regularization as supplemental supervisions. The self-reinforcement supervision is inspired by the memorization effects of DNNs and aims to correct noisy labels. Consistency regularization includes an inter-view regularization based on ensemble classifiers capable of filtering different errors, and an intra-view regularization to explore the local homogeneity of the graph [39].

Specifically, we propose to train a pair of peer GNNs to enforce adequate supervision as well as govern noise labels. First, we augment the raw graph by linking labeled and unlabeled nodes to facilitate efficient message passing, following NRGNN [6]. Then, in each epoch, we progressively perform the main division of clean and noisy candidate set by the small-loss criterion [14]. Next, a subset of confident nodes which predict a different class from their labels in the noisy candidate set is reinforced by training with their own prediction. Similarly, we extend the label set by adding those confident and consistent unlabeled nodes to the training set. Finally, we apply inter-view regularization to help two classifiers cooperatively mimic each other’s soft targets and intra-view regularization to enable nodes to learn from their neighbors.

In summary, the main contributions of our work are as follows.

- We investigate the robust training problem of GNNs from the noise governance perspective, which has been under-explored in previous studies.
- We develop a novel RTGNN model which governs label noises explicitly with self-reinforcement and consistency regularization. RTGNN also enables fine-grained learning on relatively clean, potentially noisy, and pseudo labels. This allows effectively leveraging supervision information while limiting the impact of label noises.
- We conduct extensive experiments to evaluate the effectiveness of our new approach, and the results validate the consistent superior performance of RTGNN over state-of-the-art methods with two types of noises and various noise rates.

2 RELATED WORK

2.1 Robust Deep Learning

It has been reported in [15, 22] that DNNs are prone to over-parameterize. As a result, they could overfit to and even memorize noisy labels, resulting in degraded generalization and poor performance [2, 42]. In the last few years, robust deep learning dealing with label noises is gaining more attention, especially in applications with non-graph data such as images [10, 14, 17, 24, 29, 44]. Such work can be roughly divided into two categories: sample-centric and loss-centric.

Sample-centric approaches seek to enhance the robustness of deep models by selecting clean samples for training. Malach et al. [24] proposed an update-by-disagreement strategy for sample selection, and trained two predictors simultaneously and performed parameter updates only on samples in disagreement areas of the two predictors. Inspired by the memorization effects of DNNs, Han et al. [14] developed a Co-teaching paradigm that also trains two networks such that each network samples its small-loss instances to update the parameters of its peer network. The small-loss Co-teaching paradigm has been further extended by bridging the update-by-disagreement strategy as Co-teaching+ [41] and the Co-regularization max-agreement principle as JoCoR [35]. Recently, more metrics have been explored for sample selection, e.g., loss at different stages of model fitness [16], network output at different training epochs [26], margins to decision boundaries [30], sample uncertainty [37], and divergence between different classifiers [40].

In contrast, loss-centric approaches adopt noise-robust loss functions or perform direct loss correction to combat label noises. One type of such methods aims to design loss functions that are robust to noise. Ghosh et al. [10] showed that the mean absolute error (MAE) loss is inherently robust to label noises. This idea was further extended by GCE [44] which can be viewed as a generalization of MAE and cross entropy (CE). SCE [34] boosts CE symmetrically with a noise-robust term called reverse cross entropy (RCE). The complementary loss function method [33] utilizes both CE loss and robust loss to balance learning efficiency and robustness. APL [23] classifies existing loss functions into active and passive based on their optimization behavior; it leverages active normalized loss for robust training and complements training with passive loss to address the under-fitting problem. The second type of methods is direct loss correction. Goldberger et al. [11] adopted a noise adaptation layer to model and correct the noise distribution. The F-correction method [29] proposes forward and backward correction which rectifies loss based on the noise transition matrix.

While the above methods achieved good performance in supervised training on non-graph data, our work explores a new perspective that focuses on semi-supervised learning with noisy
labels on graphs and designs a new noise governance strategy to alleviate noise impact.

2.2 Training GNNs with Noisy Labels

GNNs have achieved state-of-the-art performance on several semi-supervised benchmarking tasks, e.g., link prediction and node classification [13, 20, 31, 38]. GNNs broaden the convolution operation to graph data. They learn a graph node’s representation by aggregating the features of its neighbors. GNNs can mainly be divided into spectral-based [3, 8, 20] and spatial-based [13, 31, 38] ones. While it has been shown that deep models are vulnerable to label noises, robust training of GNNs is generally under-explored, and only a few studies investigated the robustness of GNNs with noisy labels [6, 27]. Among them, D-GNN [27] shows that GCNs could be very vulnerable to label noises, and exploits backward loss correction [29] to boost performance. However, one-step loss correction is insufficient to deal with challenging scenarios, e.g., the one with noisy and scarce labels that we consider. Close to our work is NRGNN [6], which learns a robust GNN with noisy and sparse labels; it proposes to link unlabeled nodes with labeled ones and further mine accurate pseudo-labels to provide more supervision. However, noisy labels are not explicitly governed by NRGNN, thus resulting in error propagation during message passing to some extent. Different from NRGNN, we distinguish noisy labels from clean ones and apply additional supervision and label correction to reduce the impact of label noises.

3 PRELIMINARIES

Notation and problem formulation. We represent a graph \( G = (V, A, X) \) as a triple: a vertex set \( V \), an adjacency matrix \( A \), and a node feature matrix \( X \). Without loss of generality, let the vertices of \( G \) be consecutively labeled from 1 to \( |V| \), i.e., \( V = \{1, 2, \ldots, |V|\} \). We consider undirected and unweighted graphs. Thus, the adjacency matrix \( A \in \mathbb{R}^{V \times V} \) is binary: \( A_{ij} = 1 \) if there is an edge between nodes \( i \) and \( j \), and \( A_{ij} = 0 \) otherwise. Each node is assigned with a \( d \)-dimensional feature vector. The node feature matrix \( X \in \mathbb{R}^{V \times d} \) arranges these feature vectors vertically such that the \( i \)-th row of \( X \), denoted as \( X_i \in \mathbb{R}^d \), is the feature vector of node \( i \).

We focus on robust training of GNNs for semi-supervised node classification. It assumes that the nodes of a subset \( V_L \subset V \) are assigned with labels in advance. Let \( C > 1 \) denote the number of node classes. Each node label \( Y \in \{1, \ldots, C\} \) can be alternatively represented as a one-hot vector \( y \in \{0, 1\}^C \). Recall that node labels can be scarce and noisy in practice. In other words, \( (1) \) \( |V_L| \) is significantly smaller than \( |V| \), and \( (2) \) \( Y \) might be incorrect for some of the nodes \( i \in V_L \). To tackle the node classification task, GNNs first compute a logit vector \( o^i_\theta \in \mathbb{R}^C \) for each node \( i \), where \( \theta \) is the model parameters. The probability of node \( i \) belonging to class \( j \) is then derived as:

\[
    p^{i,j}_\theta = \frac{\exp(o^{i,j}_\theta)}{\sum_{k=1}^{C} \exp(o^{i,k}_\theta)},
\]

where \( o^{i,k}_\theta \) denotes the \( k \)-th entry of \( o^i_\theta \).

Two types of label noises. We consider two types of categorical label noises: uniform and pair. These two noise types are widely adopted in the literature [6, 14, 24]. Let \( \epsilon \) denote the noise rate of node labels. For uniform noise, the labels have a probability of \( \epsilon/(C-1) \) to be uniformly flipped to other classes. For pair noise, the labels probably make mistakes only within very similar class [14], i.e., the labels have a probability of \( \epsilon \) to be flipped to the paired class. In this work, we assume that the majority of labeled nodes have correct labels, i.e., the noise rate \( \epsilon < 0.5 \).

4 METHODOLOGY

4.1 Overview

Our new RTGNN framework for Robust Training of GNNs with scarce and noisy label labels seeks to explicitly govern label noise to enable sufficient learning from clean labels while limiting the impact of noisy ones. An overview of RTGNN is given in Fig. 1.

RTGNN first augments the input graph by learning an edge predictor to infer potential links between labeled and unlabeled nodes (Sec. 4.2). These added links lead to more efficient message passing, thus mitigating the label scarcity issue. The augmented graph is then fed to a pair of peer GCNs for explicit noise governance (Sec. 4.3). Based on the prediction of the two peer GCNs, nodes are classified into different categories, enabling nodes to choose supervision strategies adaptively. More specifically, labeled nodes are divided into clean candidate set \( V_c \) and noisy candidate set \( V_n \) based on the small-loss criterion [14] (Sec. 4.3.1). The clean nodes are mainly supervised by their assigned labels. RTGNN further identifies a subset \( V_{sr} \subset V_n \) of noisy label nodes whose predictions are confident but different from their assigned labels. It then reinforces the training of nodes in \( V_{sr} \) with their own predicted labels to alleviate noise propagation (Sec. 4.3.2).

For the remaining nodes in \( V_{ns} \setminus V_{sr} \), label-based training is performed with a down-weighted loss. Similar to the self-reinforcement case, RTGNN further generates pseudo-labels for those unlabeled nodes whose predictions are confident (Sec. 4.3.3) in order to facilitate sufficient learning. Finally, it introduces the inter-view and intra-view regularizations to further prevent the model from overfitting to noise (Sec. 4.3.4). We will summarize the different categories of nodes and their supervisions in Sec. 4.4.

4.2 Graph Augmentation

Latent graph learning has shown to be beneficial in a number of graph learning tasks, owing to its flexibility to form graph structures optimized for specific tasks [5, 9, 19, 21, 28, 45]. Accordingly, we also utilize latent graph learning to densify the input graph as augmentation, to promote supervision propagation and alleviate label scarcity. Inspired by [6], we choose to infer potential links between labeled and unlabeled nodes. The reasons are two-fold: 1) labeled nodes could provide direct data supervision to similar unlabeled nodes, and 2) unlabeled nodes with pseudo-labels (Sec. 4.3.3) could facilitate model supervision on labeled ones as a supplement.

To keep the extra computational cost of graph augmentation affordable, we decouple the process into candidate generation and link inference. For candidate generation, we retrieve the top-\( K \) nearest labeled/unlabeled nodes for each unlabeled/labeled one and the distance is evaluated in the node feature space [7, 9]. The generation step can be conducted offline in advance and efficient approximation methods [12, 46] are available for large graphs.
Next, we train an encoder-decoder [21] edge predictor to infer links. A GCN [20] is utilized as the encoder to project nodes into a latent space based on both node feature and structure information:

\[ Z = \text{GCN}(X, A), \]  

(2)

We then adopt an inner-product decoder for link inference. More specifically, the predicted edge weight \( w_{ij} \) between nodes \( i \) and \( j \) is estimated as the non-negative cosine similarity between their node representations \( z^i \) and \( z^j \) learned by the encoder:

\[ w_{ij} = \max(\frac{z^i \cdot z^j}{\|z^i\| \|z^j\|}, 0). \]  

(3)

We train the edge predictor with a negative-sampling based reconstruction objective:

\[ L_{\text{rec}} = \sum_i \left( \sum_{j: A_{ij} > 0} (w_{ij} - A_{ij})^2 + N_{\text{neg}} \sum_{j' : P_n \cup \{i\}} (w_{ij'} - A_{ij'})^2 \right), \]  

(4)

where \( N_{\text{neg}} \) is the number of negative samples for each node and \( P_n \) is the distribution of negative samples (e.g., uniform). We employ negative sampling to improve computational efficiency and avoid bias towards negative node pairs. The adjacent matrix \( A \) of the augmented graph is constructed as:

\[ A_{ij} = \begin{cases} 
1 & \text{if } A_{ij} = 1; \\
\frac{w_{ij}}{\tau} & \text{if } A_{ij} = 0, j \in \text{topK}(i), \text{and } w_{ij} > \tau; \\
0 & \text{otherwise}. 
\end{cases} \]  

(5)

Note that \( \text{topK}(i) \) includes the retrieved nearest neighbor candidates for node \( i \) and the threshold \( \tau \) filters those unreliable ones.

Following [4, 6], we train an end-to-end model by jointly learning node classification and graph reconstruction. The training process will be described in Sec. 4.4.

### 4.3 Robust Training via Noise Governance

The core of RTGNN lies in explicit label noise governance. To achieve this, RTGNN feeds the augmented graph to a pair of peer GCNs that share the same architecture but have different parameters, \( \theta_1 \) and \( \theta_2 \). Based on the predictions of these two GCNs, says \( \hat{p}_{\theta_1} \) and \( \hat{p}_{\theta_2} \), RTGNN classifies the nodes into different categories and further exploits different supervision strategies accordingly. As such, RTGNN is able to effectively exploit the supervision of clean labels while limiting the impact of noisy ones.

#### 4.3.1 Labeled node division

We first divide labeled nodes of \( \mathcal{V}_L \) into clean and noisy candidate sets, \( \mathcal{V}_{cl} \) and \( \mathcal{V}_{ns} \). Previous studies have observed that DNNs follow the pattern of learning clean labels first and then gradually overfitting to noisy labels [2]. This will lead to different loss distributions for clean and noisy nodes. Fig. 2 also empirically verifies this phenomenon when training a GCN on graph data: The loss values of clean nodes are generally smaller than those of noisy nodes in the early stage. Inspired by the above observation, we adopt the small-loss criterion [14] for labeled node division. Also, here we leverage the peer GCNs as different classifiers possess different abilities to exclude noises because they form diverse decision boundaries [14, 41]. We define the mutual loss derived from cross entropy as the loss metric for a node \( i \), as:

\[ L_{\text{mutual}}^{i} = -y^i \log(p_{\theta_1}^i) - y^i \log(p_{\theta_2}^i) = -y^i \log(p_{\theta_1}^i / p_{\theta_2}^i). \]  

(6)

The mutual loss measures prediction confidence, i.e., \( L_{\text{mutual}}^{i} \) has a low value if both the GCNs classifiers correctly predict the class of node \( i \). As clean labels are easier to learn, we expect that the mutual loss values for clean label nodes are smaller than noisy ones.

Let \( T_{\text{max}} \) denote the number of training epochs. In the \( t \)-th epoch, clean and noisy candidate sets are formally divided as follows:

\[ th_{\text{epoch}}^t = \text{Percentile}(L_{\text{mutual}}^{i}, 100 - \frac{50t}{T_{\text{max}}}), \]

\[ th_{\text{avg}}^t = \text{Average}(L_{\text{mutual}}^{i}), \]

\[ \mathcal{V}_{cl} = \{ i \mid L_{\text{mutual}}^{i} < \text{max}(th_{\text{epoch}}^t, th_{\text{avg}}^t) \}, \]

\[ \mathcal{V}_{ns} = \mathcal{V}_L \setminus \mathcal{V}_{cl}. \]  

(7)
Notes: (1) Percentile ($L, p$) is the value below which $p\%$ of the loss values in $L$ fall, (2) thresholds $th^l_{\text{epoch}}$ and $th^l_{\text{any}}$ are the upper bounds of loss values for clean label nodes, (3) at least half of labeled nodes are classified as clean given a noise rate $\epsilon < 0.5$, and (4) the threshold $th^l_{\text{any}}$ further ensures that small-loss nodes are clean regardless of their relative ranks.

The training on nodes in $\mathcal{V}_l$ is supervised by their assigned labels, with $L^l_{\text{mutual}}$ being the classification loss. On the other hand, we leverage different supervisions for nodes in $\mathcal{V}_{ps}$, which will be discussed in the following subsections. The above node division strategy has two advantages. First, it does not require hyper-parameters, thus avoiding elaborate parameter tuning. Second, it strikes a balance between sufficient training in the early stage and noise-resistant training in the later stage. At the early stage of training (e.g., the first few epochs), the model is underfitting and has not yet learned reliable patterns. By choosing a conservative (i.e., high) $th^l_{\text{epoch}}$, the majority of labeled nodes are classified as clean to guide model supervision. This can also be viewed as warm-up training. Besides, as mentioned before, the memorization effect of neural networks enables one to learn from clean labels first, despite the existence of noise. Thus, choosing a conservative $th^l_{\text{epoch}}$ would not hurt the model performance. When training goes on, we progressively exclude nodes with large loss from $\mathcal{V}_l$, which prevents our model from overfitting to noise in the later stage.

4.3.2 Self-reinforcement supervision. As the labels of nodes in $\mathcal{V}_{ns}$ are prone to be noisy, RTGNN turns to other supervisions instead. We identify a subset $\mathcal{V}_{sr} \subseteq \mathcal{V}_{ns}$ of nodes on which the predictions of the two peer GCNs are confident but different from their labels. Formally, $\mathcal{V}_{sr}$ includes the nodes that satisfy:

$$Z^i = \arg \max_c p^c_{\hat{y}^i}, \quad \text{where } Y^i \neq \hat{y}^i \land \arg \max_c p^c_{\hat{y}^i} \neq Y^i,$$

where $Y^i \in \{1, \ldots, C\}$ denotes the label for node $i$. The threshold $1 - \frac{C - 1}{C \cdot T_{\text{max}}}$ linearly decreases with the increment of $t$ and is finally reduced to $1/C$. In other words, we gradually allow more nodes to self-reinforce the training.

In each epoch, we update $\mathcal{V}_{sr}$ and further compute an adaptive training weight for each node $i \in \mathcal{V}_{sr}$:

$$\mu(i) = \frac{1}{\sqrt{p^i_{\hat{y}^i} \cdot p^i_{\hat{y}^i} \cdot \sqrt{1 - \frac{C - 1}{C \cdot T_{\text{max}}}}}}, \quad L^i_{\text{sr}} = - \mu(i) z^i \log(p^i_{\hat{y}^i} \cdot p^i_{\hat{y}^i}),$$

where $z^i \in \{0, 1\}^C$ is the corresponding one-hot representation of the predicted label $Z^i$, and $\mu(i)$ serves as an adaptive learning rate. Notes: (1) $\mu(i)$ relies on the node-wise prediction confidence. (2) The scaling exponent $(1 - t/T_{\text{max}})$ gradually decreases to enlarge $\mu(i)$ in the later training stage.

4.3.3 Pseudo labeling. Learning from pseudo-labels may further ease the training with scarce and noisy labels [6]. Similarly, we select a subset $\mathcal{V}_{ps} \subset \mathcal{V} \setminus \mathcal{V}_l$ of unlabeled nodes with confident and consistent predictions to generate pseudo-labels. Formally, $\mathcal{V}_{pse}$ includes the nodes that satisfy:

$$\hat{Z}^i = \arg \max_c p^c_{\hat{y}^i} = \arg \max_c p^c_{\hat{y}^i} \cdot \sqrt{p^i_{\hat{y}^i} \cdot p^i_{\hat{y}^i} \cdot Z^i} > th_{\text{pse}}.$$

where $th_{\text{pse}}$ refers to the confidence threshold. The training on nodes in $\mathcal{V}_{pse}$ is then supervised by their pseudo-labels.

4.3.4 Consistency regularization. For nodes in $\mathcal{V}_l \cup \mathcal{V}_{pse}$, we further add some regularization to prevent overfitting. Inspired by mutual learning [43], we let the two peer GCNs mimic each other’s prediction. In this way, they teach and learn from each other. Here we use $D_{KL}$ (Kullback-Liebler divergence) as the mimicry loss:

$$L^i_{\text{inter}} = D_{KL}(p^i_{\hat{y}^i} \| p^i_{\hat{y}^i}) + D_{KL}(p^i_{\hat{y}^i} \| p^i_{\hat{y}^i}).$$

Moreover, we follow the local consistency (a.k.a. homophily [25]) assumption that linked nodes tend to belong to the same classes. This leads to a regularization term that enforces nodes to mimic neighbors’ predictions within the same GCN:

$$L^i_{\text{intra}} = \sum_j \hat{A}_{ij}(D_{KL}(p^j_{\hat{y}^i} \| p^j_{\hat{y}^i}) + D_{KL}(p^j_{\hat{y}^i} \| p^j_{\hat{y}^i})).$$

The final regularization loss is composed as:

$$L^i_{\text{reg}} = L^i_{\text{inter}} + L^i_{\text{intra}}.$$

4.4 The Overall Training Loss

Combining all together, the loss of labeled nodes can be unified as:

$$L_{\text{labeled}} = - \frac{1}{|\mathcal{V}_l|} \sum_{i \in \mathcal{V}_l} \{\zeta(i) \hat{y}^i \log(p^i_{\hat{y}^i} \cdot p^i_{\hat{y}^i}) + \lambda L^i_{\text{reg}}\},$$

where

$$\zeta(i) = 1, \quad \hat{y}^i = y^i \quad \text{if } i \in \mathcal{V}_l;$$
$$\zeta(i) = \mu(i), \quad \hat{y}^i = Z^i \quad \text{if } i \in \mathcal{V}_{sr};$$
$$\zeta(i) = \gamma \in (0, 1), \quad \hat{y}^i = \gamma y^i \quad \text{if } i \in \mathcal{V}_{ns} \setminus \mathcal{V}_{sr}.$$
### Table 2: Comparison of node classification performance (test accuracy, mean±std, averaged by 5 runs) by different models. The best results are marked in bold, and the best baseline results are underlined.

| Dataset     | Model    | Uniform Noise |       |       |       |       |       |       |       |       |       |
|-------------|----------|---------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
|             |          | 10%           | 20%   | 30%   | 40%   | 10%   | 20%   | 30%   | 40%   |       |       |
| Cora        | GCN      | 79±0.3        | 76±0.5 | 68±0.9 | 61±3.0 | 79±0.4 | 75±1.4 | 67±1.0 | 59±3.6 |       |       |
|             | Co-teaching | 79±0.4       | 77±0.3 | 69±0.7 | 62±1.8 | 80±0.5 | 76±0.8 | 67±1.0 | 63±0.8 |       |       |
|             | JoCoR    | 79±0.2        | 76±0.9 | 72±1.4 | 68±2.5 | 80±0.3 | 77±0.6 | 69±1.2 | 64±0.9 |       |       |
|             | SCE      | 78±0.4        | 77±0.8 | 69±0.9 | 60±3.4 | 80±0.5 | 77±1.0 | 67±2.4 | 57±1.3 |       |       |
|             | APL      | 79±0.4        | 74±0.6 | 69±2.1 | 59±3.2 | 80±0.5 | 75±2.3 | 67±0.9 | 59±2.2 |       |       |
|             | D-GNN    | 76±0.1        | 74±0.7 | 71±2.0 | 61±0.6 | 78±0.9 | 76±0.4 | 68±1.2 | 59±1.6 |       |       |
|             | NRGNN    | 81±0.4        | 80±1.2 | 76±0.7 | 73±1.9 | 81±0.4 | 79±0.8 | 75±1.1 | 68±1.6 |       |       |
|             | RTGNN (ours) | 82±0.7    | 80±0.2 | 79±1.0 | 78±1.1 | 82±0.3 | 80±0.6 | 77±0.6 | 72±1.4 |       |       |
| Citeseer    | GCN      | 69±0.7        | 69±0.4 | 63±1.2 | 55±1.0 | 69±0.5 | 67±0.8 | 58±1.1 | 57±1.6 |       |       |
|             | Co-teaching | 72±0.3       | 69±1.0 | 69±0.6 | 56±1.4 | 72±0.5 | 69±1.3 | 60±1.7 | 57±2.4 |       |       |
|             | JoCoR    | 72±0.3        | 71±0.7 | 69±1.3 | 58±1.2 | 72±1.0 | 69±0.4 | 64±2.5 | 58±1.6 |       |       |
|             | SCE      | 70±0.4        | 69±0.7 | 64±1.6 | 56±1.4 | 71±1.2 | 68±0.8 | 59±0.6 | 57±1.0 |       |       |
|             | APL      | 70±0.6        | 69±0.6 | 65±1.6 | 56±2.0 | 71±3.4 | 68±1.0 | 59±0.7 | 57±1.5 |       |       |
|             | D-GNN    | 71±0.3        | 68±0.7 | 63±1.0 | 54±0.9 | 70±0.5 | 69±0.5 | 62±0.6 | 56±4.0 |       |       |
|             | NRGNN    | 72±0.8        | 72±0.8 | 68±1.1 | 63±1.3 | 72±8.0 | 70±0.8 | 65±0.3 | 58±3.4 |       |       |
|             | RTGNN (ours) | 74±0.6    | 71±0.6 | 70±0.9 | 66±1.7 | 74±6.0 | 71±8.0 | 67±0.8 | 62±1.6 |       |       |
| BlogCatalog | GCN      | 69±0.7        | 66±0.4 | 65±0.9 | 53±0.9 | 69±0.4 | 62±0.5 | 58±1.0 | 57±1.2 |       |       |
|             | Co-teaching | 70±0.3       | 69±0.5 | 67±0.6 | 53±0.6 | 70±0.7 | 63±0.9 | 58±1.0 | 57±1.5 |       |       |
|             | JoCoR    | 70±0.4        | 69±0.4 | 69±1.1 | 63±1.1 | 70±5.0 | 66±1.1 | 59±1.1 | 58±2.2 |       |       |
|             | SCE      | 70±0.5        | 67±0.8 | 65±0.9 | 65±1.0 | 69±4.7 | 63±1.4 | 60±1.0 | 57±0.9 |       |       |
|             | APL      | 70±0.5        | 69±0.4 | 68±0.6 | 58±0.9 | 70±3.6 | 68±0.8 | 61±1.1 | 58±2.7 |       |       |
|             | D-GNN    | 70±0.3        | 67±0.9 | 65±0.5 | 58±0.7 | 70±1.5 | 67±1.1 | 61±1.3 | 58±4.1 |       |       |
|             | NRGNN    | 71±0.4        | 70±3.1 | 69±0.9 | 67±0.3 | 69±9.7 | 67±1.0 | 60±1.0 | 58±3.2 |       |       |
|             | RTGNN (ours) | 71±2.3    | 70±0.4 | 70±2.4 | 68±0.1 | 71±2.4 | 70±0.8 | 65±2.0 | 63±1.5 |       |       |

### 5 EXPERIMENTS

#### 5.1 Experiment Setup

**Datasets.** We conduct experiments on two citation datasets [18] (Cora and Citeseer) and a social network dataset BlogCatalog [36] to evaluate the performance of RTGNN. The dataset statistics are summarized in Table 1. To study the robustness of GNNs with scarce and noisy labels, each dataset is randomly split into 5%, 15%, and 80% for training, validation, and test, respectively. Moreover, following [6], we further randomly corrupt a fraction of labels, say $\epsilon$, in the training and validation sets. Recall in Sec. 3 that we consider two types of noises. Each dataset thus has two corrupted versions corresponding to uniform and pair noises, respectively.

**Implementation details.** We adopt a 2-layer GCN [20] with 128 hidden units as the backbone GNN model. For graph augmentation, we use a GCN with 64 hidden units as the encoder of edge predictor, fix $N_{neg}$ = 100 for negative sampling, and set threshold $\tau = 0.05$ on all datasets. The regularization loss weight $\lambda = 0.1$ for all datasets.

Moreover, we search the $K$ for nearest neighbor candidate (the topK operation in Eq. (5)) in $[25, 50, 100]$, the pseudo label threshold $t_{\text{false}}$ in $[0.7, 0.8, 0.9, 0.93]$, the reconstruction loss weight $\sigma$ in $[0.03, 0.1, 0.3, 1]$, and the down-weighted factor $\gamma$ of noisy samples in $[0.01, 0.1]$ based on the validation performance. Finally, we train our model for a total of 200 epochs with a learning rate of 0.001 and a weight decay of 5e-4. To avoid over-fitting, we also apply dropout with a dropout rate of 0.5. In the cases when quantitative measurements are reported, the test was repeated over 5 times and the average is reported$^1$. Notice that both GCNs could be used for inference, and in the experiments, we use the first one.

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$^1$Codes are available at https://github.com/GhostQ99/RobustTrainingGNN.
and varying noise rates. The results are reported in Table 2 and we observe the following from these results.

- Compared with GCN [20], loss-centric methods SCE, APL, and D-GNN perform even worse in some scenarios (e.g., SCE on Cora with 40% pair noise, APL on Cora with 40% uniform noise, and D-GNN on Citeseer with 40% pair noise). It indicates that leveraging a single robust loss function or loss correction method is insufficient. Differently, RTGNN explicitly divides nodes into several categories and adopts different training strategies accordingly.
- Compared with GCN, both Co-teaching and JoCoR yield stable and superior performance. This verifies that co-training two networks can mutually suppress the effects of noise, inspiring us to borrow the peer network architecture in our model. It also validates that performing explicit governance of clean and noisy labels is beneficial.
- JoCoR attains an overall better performance than Co-teaching by jointly training two peer networks together. This motivates us to fuse the training of two peer networks. Moreover, our RTGNN works even better, because we further leverage the model’s own ability to rectify the noisy labels. Besides, we complement the training with confident and consistent pseudo labels.
- NRGNN links unlabeled nodes with similar labeled nodes and adds pseudo-labels to mitigate the negative effect of noise. This strategy helps to bring effective supervision to unlabeled nodes. However, it might not perform well under higher noise rates since a large number of erroneous supervisions are propagated to a wide scope. To address this issue, we propose explicit noise governance to identify potentially noisy labels and alleviate their impacts. We consider our labeled node division as a primary module in RTGNN, with other types of supervisions being introduced to further boost the performance. **Overall, RTGNN consistently performs better than all baselines on three datasets with both types of noises and varying noise rates.**

### 5.3 Impacts of Training Label Rates

We next examine how our RTGNN performs with different fractions of training labels. For this purpose, we split the datasets into x%, (20 – x)%, and 80% for training, validation, and test, respectively. Since we focus on training GNNs with sparse and noisy labels, we vary x from 2.5 to 10 and evaluate the test node classification accuracy. The results on Cora and Citeseer with 30% noise rate are reported in Fig. 3 and Fig. 4. Note that results are similar with other noise rates and we observe the following.

- Our proposed RTGNN consistently outperforms all baselines. Even under an extremely low label rate (x = 2.5%), our model achieves favorable performances by leveraging the supervision of clean labels while restricting that of noisy ones.
- Compared using the low (2.5%) and high (10%) label rates, we observe that our model makes a bigger improvement upon the competitive NRGNN baseline with high (10%) label rates. As we mentioned before, without explicit noise governance, NRGNN mix-ups the propagation of clean and noisy labels in graphs, thus being severely affected by the increasing size of noisy labels.

### 5.4 Ablation Study

#### 5.4.1 Ablation study on graph augmentation.

To validate the effect of the graph augmentation module, we plug it into a GCN. In addition to the cross entropy (CE) loss, various loss functions are also tested. As in Eq. (16), we train the augmented baselines by jointly training two networks together. This motivates us to borrow the peer network architecture in our model. It also validates that performing explicit governance of clean and noisy labels is beneficial. A sparse graph (Citeseer) gains more benefits than a denser one (BlogCatalog). On a dense graph, unlabeled nodes receive sufficient but probably wrong supervision from labeled neighbors. Without an appropriate strategy to govern label noise, the chance for unlabeled nodes to receive correct supervision isn’t significantly increased, thus yielding limited performance improvement.
This suggests that developing an effective noise governance strategy can largely help deal with graphs of different densities.

5.4.2 Ablation study on noise governance. We further investigate how each sub-module in our noise governance strategy contributes to the overall performance of RTGNN. For simplicity, we denote these sub-modules as follows.

- LD: Labeled node division (introduced in Sec. 4.3.1).
- SR: Self-reinforcement supervision (introduced in Sec. 4.3.2). It is an operation following labeled node division.
- PL: Pseudo labeling (introduced in Sec. 4.3.3).
- CR: Consistency regularization (introduced in Sec. 4.3.4).

We set the label rate as $x = 5\%$, and present the results in Table 4. From these results, we observe the followings.

- The RTGNN model without our labeled node division (LD) performs the worst. In particular, under 40% pair noise, it drops by 2.4% on Citeseer and by 5.1% on BlogCatalog. This indicates the importance of dividing labeled nodes into clean and noisy candidate sets and leveraging different training strategies for them. Meanwhile, the effectiveness of our designed labeled node division strategy is also validated.
- Self-reinforcement supervision (SR) further exploits the neural network’s ability for reinforcing itself with rectified labels, thus attaining more accurate supervision.
- Pseudo labeling (PL) enhances the performance because it serves as a kind of complementary supervision.
- Consistency regularization (CR) further prevents nodes from overfitting to noise by combining two classifiers to exclude noise together and exploiting local homogeneity in the graph.

| Dataset | Variants | Uniform Noise | Pair Noise |
|---------|----------|---------------|------------|
|         |          | 30% | 40%       | 30% | 40% |
| Citeseer | w/o LD, SR | 69.5±0.8 | 64.0±1.3 | 66.2±0.7 | 59.7±1.3 |
|         | w/o SR   | 70.3±0.9 | 65.1±1.3 | 67.2±0.7 | 61.1±1.5 |
|         | w/o PL   | 70.5±1.2 | 65.7±1.5 | 67.3±1.7 | 61.4±1.8 |
|         | w/o CR   | 70.6±1.0 | 65.4±2.1 | 67.5±1.2 | 61.2±1.9 |
|         | All      | 70.9±0.7 | 66.0±1.7 | 67.8±0.8 | 62.1±1.6 |

| BlogCatalog | w/o LD, SR | 69.2±0.5 | 67.1±0.6 | 61.4±0.5 | 58.5±1.2 |
|             | w/o SR   | 70.1±0.4 | 67.5±0.9 | 64.5±1.2 | 62.0±1.3 |
|             | w/o PL   | 70.4±0.4 | 67.5±1.3 | 64.6±1.1 | 62.9±2.0 |
|             | w/o CR   | 70.3±0.2 | 67.8±1.1 | 64.4±1.4 | 62.5±1.7 |
|             | All      | 70.7±0.4 | 68.0±1.1 | 65.2±1.0 | 63.6±1.5 |

5.5 Sensitivity Analysis of Hyper-parameters

In this section, we conduct experiments to examine the impact of several important hyper-parameters in our model. The label rate is set as $x = 5\%$ and the noise rate is set as 30% and 40% as examples. We report the average results of 5 runs.

We consider the following key hyper-parameters. (1) In Fig. 5(a) and Fig. 5(b), we show the impact of the graph reconstruction loss weight $\alpha$. On Citeseer, RTGNN achieves the best results in most cases when $\alpha = 0.03$. On BlogCatalog, RTGNN achieves the best results when $\alpha = 1$ for all the cases. (2) In Fig. 5(c) and Fig. 5(d), we show the impact of the edge threshold $\tau$. When $\tau = 0$, noisy edges may be introduced, and when $\tau$ becomes too large, some potential links would not be identified. On Citeseer, RTGNN achieves the best results when $\tau = 0.05$ for all the cases. On BlogCatalog, RTGNN achieves the best results in most cases when $\tau = 0.05$. (3) In Fig. 5(e) and Fig. 5(f), we show the impact of the consistency regularization weight $\lambda$. RTGNN achieves the best result when $\lambda = 0.2$ on Citeseer under 30% uniform and pair noise and $\lambda = 0.1$ on Citeseer under 40% uniform and pair noise. In general, $\lambda = 0.1$ gives good performances for various scenarios on Citeseer. RTGNN achieves the best results when $\lambda = 0.1$ on BlogCatalog for all cases.

6 CONCLUSIONS

In this paper, we investigated how to train a robust GNN classifier with scarce and noisy node labels. We proposed a novel RTGNN framework which performs explicit noise governance with supplemental supervision. Specifically, we classified labeled nodes into clean and noisy ones and adopted reinforcement supervision to correct noisy labels. We also created pseudo labels to provide extra training signals. Moreover, we leveraged consistency regularization to prevent overfitting to noise. By doing so, RTGNN could enable sufficient learning from clean labels while limiting the impact of noisy ones. Comprehensive experiments on three widely-used datasets showed superior performance of RTGNN under two types of noise and varying noise rates. We expect that our work would inspire more studies on robust semi-supervised learning on graphs.
