GlnK Facilitates the Dynamic Regulation of Bacterial Nitrogen Assimilation

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ABSTRACT Ammonium assimilation in Escherichia coli is regulated by two paralogous proteins (GlnB and GlnK), which orchestrate interactions with regulators of gene expression, transport proteins, and metabolic pathways. Yet how they conjointly modulate the activity of glutamine synthetase, the key enzyme for nitrogen assimilation, is poorly understood. We combine experiments and theory to study the dynamic roles of GlnB and GlnK during nitrogen starvation and upshift. We measure time-resolved in vivo concentrations of metabolites, total and posttranslationally modified proteins, and develop a concise biochemical model of GlnB and GlnK that incorporates competition for active and allosteric sites, as well as functional sequestration of GlnK. The model predicts the responses of glutamine synthetase, GlnB, and GlnK under time-varying external ammonium level in the wild-type and two genetic knock-outs. Our results show that GlnK is tightly regulated under nitrogen-rich conditions, yet it is expressed during ammonium run-out and starvation. This suggests a role for GlnK as a buffer of nitrogen shock after starvation, and provides a further functional link between nitrogen and carbon metabolisms.

INTRODUCTION

To adapt to the highly variable nutrient conditions in their natural habitat, microorganisms have evolved a complex intracellular circuitry coupling signal transduction, membrane transport, gene expression, and metabolism. A widely conserved example is the ammonium assimilatory system in Escherichia coli, which coordinates the uptake of nitrogen with other pathways involved in carbon assimilation and maintenance of cellular energy status (1–3). External ammonium (E. coli’s preferred nitrogen source) is assimilated into glutamate and glutamine in two steps: first, ammonium and intracellular glutamate are converted into glutamine (GLN) in a reaction catalyzed by the enzyme glutamine synthetase (GS); second, GLN is combined with α-ketogluterate (α-KG), a product of carbon metabolism, to yield two molecules of glutamate (for a net production of one glutamate molecule) in a reaction catalyzed by the enzyme glutamate synthase (Fig. 1).

Although glutamine and glutamate are both key intermediates toward the production of amino acids and nucleotides, their wider roles in cellular metabolism are different. Whereas glutamate is the nitrogen source for most (88%) reactions in the cell (1), glutamine constitutes the primary signal controlling the activity of enzymes in the ammonium assimilation system. As a result, their regulatory requirements are different: homeostatic regulation of glutamate is essential to maintain growth rate, whereas glutamine levels must adjust rapidly to reflect cellular nitrogen status while at the same time remaining within physiologically acceptable bounds. In particular, when nutrient-rich conditions are suddenly restored after a period of starvation, the cell must be able to avoid glutamine shock (4,5).

The modulation of GS activity is the primary means by which E. coli achieves these regulatory targets in the face of changing nitrogen levels. On the one hand, as extracellular ammonium is used up during growth, the activity and abundance of GS is raised to maintain the growth rate as long as possible. On the other hand, when favorable conditions are suddenly restored, GS can be turned off. This nonlinear response of GS is controlled by the bifunctional enzyme adenylyl-transferase/adenylyl-removase (AT/AR), which can reversibly adenylylate (inactivate) or deadenylylate (activate) independently each of the 12 monomers that...
conform GS, thus modulating GS activity in a graded manner (6). The activity of AT/AR is in turn regulated allosterically by glutamine and by two highly similar signal transduction proteins, GlnB and GlnK (encoded, respectively, by the \textit{glnB} and \textit{glnK} genes) (2,7). Importantly, GlnB and GlnK share a source of upstream regulation, themselves being reversibly uridylylated by a second bifunctional enzyme, uridyl-transferase/uridylyl-removase (UT/UR), which enables GlnB and GlnK to control the enzyme AT/AR (8). Specifically, under glutamine limitation GlnB and GlnK are mostly uridylylated, leading to increased AR activity and inhibition of AT activity (Fig. 1). In addition to regulating AT/AR, GlnB and GlnK also regulate the expression of GS and bind \(\alpha\)-KG, communicating with carbon metabolism and signal transduction pathways (2).

Due to the apparent redundancy of having two signaling proteins (GlnB and GlnK) relaying the glutamine state of the cell, previous models (9–12) have ignored GlnK regulation of AT/AR, it being less potent than GlnB. This simplification is supported by mutational studies of the receptor interaction domains of GlnB and GlnK (13) and by in vitro studies (14). From this viewpoint, the role of GlnK is mostly circumscribed to regulating the membrane-bound channel protein AmtB, whose gene (\textit{amtB}) lies in the same operon as \textit{glnK}, causing \textit{glnK} and \textit{amtB} expression to be directly correlated (15–17).

However, various experiments suggest that GlnK also acts as an effective regulator of AT/AR. For instance, GlnB-deficient strains (i.e., \(\Delta\text{glnB}\) mutants) exhibit unimpaired growth (18) with regulated GS (de)adenylylation (19), suggesting that GlnK can substitute for GlnB. It has also been found that GlnK does interact with AT/AR in vitro (14), albeit relatively weakly, and binds \(\alpha\)-KG, ATP, and ADP similarly to GlnB (20,21). Importantly, \textit{glnK} expression is induced during nitrogen limitation, whereas \textit{glnB} is expressed constitutively (19). Taken together, these observations raise questions about the in vivo regulation of AT/AR and about a complementary role for GlnK in nitrogen assimilation to provide not only added redundancy but also a flexible and rapid response to the consequences of variations in external ammonium levels.

To establish the relevance of GlnK in nitrogen regulation during external nitrogen variations, we combined experiment with modeling. We measured the growth rate (Fig. 2) and the in vivo temporal response of relevant metabolites, proteins, and posttranslational modification (PTM) protein states during ammonium run-out, starvation, and a subsequent ammonium shock (Fig. 3). Measurements of the wild-type (WT) strain were complemented with experiments with two genetic knock-outs: \(\Delta\text{glnB}\) (no GlnB) and \(\Delta\text{glnK}\) (no GlnK), as shown in Fig. 5.

Our experiments show that growth rate and ammonium uptake are not impaired by the removal of either GlnB or GlnK (Fig. 2), suggesting that GlnB and GlnK form two complementary branches of nitrogen signal transduction regulating AT/AR. We also find that GlnK plays a limited role in regulating GS expression and adenylylation during ammonium assimilation.
GlnK is expressed before and during starvation to temporarily alleviate excess ammonium import and assimilation when ammonium becomes available again.

**MATERIALS AND METHODS**

**Strains and growth conditions**

Experiments were performed with *E. coli* K12 (NCM3722) (23). NCM3722ΔglnB in-frame deletions were obtained through P1 phase transduction (24), using strain JW2537 with the glnK knock-out from the Keio collection as the donor strain (25). NCM3722ΔglnB was verified by genomic locus sequencing. Precultures were grown in Gutnick minimal media, supplemented with 10 mM NH₄Cl, 0.4% (w/v) glucose, and Ho-Le trace elements. Main cultures were inoculated in same media but with limiting 3 mM NH₄Cl, resulting in NH₄Cl starvation at mid log phase. Ammonium depletion and optical density (OD) OD₆₀₀ were determined at defined time points during the course of experiments as described by Schumacher et al. (26). After one generation time (40 min) of growth arrest, NH₄Cl was added to obtain a concentration of 3 mM (upshift).

**Metabolite and protein measurements**

Glutamine and α-ketoglutarate were quantified using liquid chromatography-mass spectrometry and nuclear magnetic resonance, as described in Schumacher et al. (26) and Komorowski et al. (27). Total abundance and uridylylation level of GlnK were determined using multiple reaction monitoring mass-spectrometry (MRM-MS) (28) with absolute standard protein quantification (26,29). Briefly, isotopically labeled GlnK protein standard was purified after IPTG-induced overexpression in *E. coli* harboring JW0440 from the ASKA(λ) collection (glnK) (30), grown in the presence of labeled L-arginine (13C₆, 15N₄) and L-Lysine (13C₆, 15N₂). Ni-affinity purified GlnK standard purity was judged visually by SYPRO Ruby Protein Gel Stain (Invitrogen, Carlsbad, CA) stained SDS-PAGE to be >90% and with GlnK standard concentration determined. Isotopic labeling efficiency was determined by MRM-MS to be 100%. Total GlnK abundances were determined by the ratio of MRM-MS signals of GlnK unlabeled/labeled signature peptides, excluding the uridylylation site peptide (Table S1) and undetermined by the ratio of MRM-MS signals of GlnK unlabeled/labeled signature peptides, excluding the uridylylation site peptide (Table S1) and intracellular concentrations calculated (26). GlnK uridylylation levels were directly measured by the abundance of the uridylylated GlnK peptide GAEYS(Ump)VNFLPK compared with the nonuridylylated peptide GAEYSVNFLPK. The GlnK protein concentrations derived from nonuridylylated peptides correspond well with GlnK protein concentrations derived independently from the sum of uridylylated and nonuridylylated peptide GAEYSVNFLPK (Fig. S8). A similar procedure is used for quantifying GlnB and GS and their PTMs (27).

**Description of the model**

The schematic of the system regulating nitrogen assimilation in *E. coli* is shown in Fig. 1. We use three coupled nonlinear ordinary differential equations (ODEs) to describe the dynamics of the monomeric concentrations of uridylylated GlnB, uridylylated GlnK, and adenylylated GS as follows:

\[
\begin{align*}
\frac{d[GlnB-U]}{dt} &= v_{UT,GlnB} - v_{UR,GlnB} \\
\frac{d[GlnK-U]}{dt} &= v_{UT,GlnK} - v_{UR,GlnK} \\
\frac{d[GS-A]}{dt} &= v_{AT,GS} - v_{AR,GS-A},
\end{align*}
\]

where *v* is the reaction rate constant, and *GlnB*, *GlnK*, and *GS* represent the monomeric concentrations of glutamine and α-ketoglutarate synthase, respectively.
where the right-hand side contains the balance of fluxes corresponding to (de)uridylylation and (de)adenylylation of the corresponding proteins. These fluxes contain several kinetic parameters and depend nonlinearly on the concentrations of substrates, products and allosteric effectors. We now describe these terms in detail.

Equations for UT/UR

The UT and UR activities in the bifunctional enzyme UT/UR are treated as independent, unidirectional reactions obeying Michaelis-Menten kinetics. Due to the specificity of UT/UR active sites (31), GlnB and GlnK are modeled as competitive substrates. Our model considers only the experimentally measured monomeric concentration of the uridylylated species, and disregards the multimeric nature of GlnB and GlnK, because (de)uridylylation of GlnB monomers is noncooperative (32). GLN acts as an allosteric activator to UR and an inhibitor to UT activities (8). These can be encapsulated in the following rate equations (see Supporting Material for derivations):

\[
\begin{align*}
V_{\text{UT}, \text{GlnB}} &= \frac{[\text{GlnB}]}{K_{m, \text{GlnB}}} \left(1 + \frac{[\text{GlnB}]}{K_{m, \text{GlnB}}} + \frac{[\text{GlnK}]}{K_{m, \text{GlnK}}} \left(1 + \frac{[\text{GLN}]}{K_{\text{GLN},1}}\right)\right), \\
V_{\text{UR}, \text{GlnB-U}} &= \frac{[\text{GlnB-U}]}{K_{m, \text{GlnB-U}}} \left(1 + \frac{[\text{GlnB-U}]}{K_{m, \text{GlnB-U}}} + \frac{[\text{GlnK-U}]}{K_{m, \text{GlnK-U}}} \left(1 + \frac{[\text{GLN}]}{K_{\text{GLN},1}}\right)\right), \\
V_{\text{UT}, \text{GlnK}} &= \frac{[\text{GlnK}]}{K_{m, \text{GlnK}}} \left(1 + \frac{[\text{GlnB}]}{K_{m, \text{GlnB}}} + \frac{[\text{GlnK}]}{K_{m, \text{GlnK}}} \left(1 + \frac{[\text{GLN}]}{K_{\text{GLN},1}}\right)\right), \\
V_{\text{UR}, \text{GlnK-U}} &= \frac{[\text{Glnk-U}]}{K_{m, \text{GlnK-U}}} \left(1 + \frac{[\text{GlnB-U}]}{K_{m, \text{GlnB-U}}} + \frac{[\text{GlnK-U}]}{K_{m, \text{GlnK-U}}} \left(1 + \frac{[\text{GLN}]}{K_{\text{GLN},1}}\right)\right).
\end{align*}
\]

Here \(V_\cdot\) and \(K_{m,\cdot}\) are the maximal rates and Michaelis constants of the (de) uridylylation reactions, and \(K_{\text{GLN},1}\) is the binding affinity of GLN to the allosteric site of UT/UR. The concentration of GlnB (and similarly GlnK) is obtained from the conservation relation, as follows:

\[
[\text{GlnB}] = [\text{GlnB}_{\text{total}}](t) - [\text{GlnB-U}],
\]

where the total concentration is a time-varying experimental measurement (Fig. 3).

Sequestration of GlnK

We assume that GlnK-AmtB complex formation regulates the amount of GlnK accessible to other reactions, and is controlled by \(\alpha\)-KG following a Hill-type form (17):

\[
[\text{GlnK}] = [\text{GlnK}_{\text{total}}] \left(1 - \frac{[\alpha\text{-KG}]^{n_H}}{K_{\alpha\text{-KG},1} + [\alpha\text{-KG}]^{n_H}}\right),
\]

where \([\text{GlnK}_{\text{total}}]\) and \([\text{GlnK}]\) are the total and accessible concentrations of GlnK, respectively, \(K_{\alpha\text{-KG},1}\) is the dissociation constant for \(\alpha\)-KG; \(n_H\) is the Hill-coefficient; and \(x\) is the minimum concentration of accessible GlnK, which indicates the ratio of AmtB to GlnK. If \([\alpha\text{-KG}] < < K_{\alpha\text{-KG},1}\), then \([\text{GlnK}] = x[\text{GlnK}_{\text{total}}]\), and the maximal amount of GlnK is sequestered; if \([\alpha\text{-KG}] >> K_{\alpha\text{-KG},1}\), then \([\text{GlnK}] \approx x[\text{GlnK}_{\text{total}}]\), so no GlnK is sequestered.

Equations for AT/AR

We split the activity of AT/AR into independent AT and AR reactions, both obeying Hill-type kinetics. We consider that GlnB-U/GlnK-U and GlnB/GlnK are pairwise competing for allosteric sites, whereas glutamine can bind independently to a third allosteric site (7,21,33). The binding of GlnB and \(\alpha\)-KG are synergistic, and that of GlnB-U and \(\alpha\)-KG are antagonistic (34), leading to the following activation parameters:

\[
K_{\text{GlnB}} = K_{\text{GlnB}} \left(1 + \frac{[\alpha\text{-KG}]^{n_H}}{K_{\alpha\text{-KG},2}}\right),
\]

\[
K_{\text{GlnB-U}} = K_{\text{GlnB-U}} \left(1 + \frac{[\alpha\text{-KG}]^{n_H}}{[\alpha\text{-KG}]^{n_H}}\right).
\]

Similar expressions are used for GlnK and GlnK-U. As above, we only describe GS-A monomers (without explicit GS-A complexes) (9,35,36). We neglect retroactivity from GlnB and GlnK on \(\alpha\)-KG, because the latter is two orders of magnitude more abundant, and from AT/AR on GlnB and GlnK, because GlnK level is expected to be significantly higher (7). These assumptions result in the following rate equations (see Supporting Material for a detailed derivation):

\[
V_{\text{AT}} = \frac{V_{\text{AT}}[\text{GS}]^{p_{\text{AT}}}}{K_{m,\text{GS}}^{p_{\text{AT}}} + [\text{GS}]^{p_{\text{AT}}}} \left[\frac{1}{1 + \frac{K_{\text{GlnB}}}{[\text{GlnB}]} + \frac{K_{\text{GlnB}}}{[\text{GlnK}]} + \frac{K_{\text{GlnB}}}{[\text{GlnK}]} \left(1 + \frac{[\text{GLN}]}{K_{\text{GLN},2}}\right)}\right] + \frac{1}{1 + \frac{K_{\text{GlnK}}}{[\text{GlnK}]} + \frac{K_{\text{GlnK}}}{[\text{GlnK}]} \left(1 + \frac{[\text{GLN}]}{K_{\text{GLN},2}}\right)}
\]

\[
V_{\text{AR}} = \frac{V_{\text{AR}}[\text{GS-A}]^{p_{\text{AR}}}}{K_{m,\text{GS-A}}^{p_{\text{AR}}} + [\text{GS-A}]^{p_{\text{AR}}}} \times \left[\frac{1}{1 + \frac{K_{\text{GlnB-U}}}{[\text{GlnB-U}]} + \frac{K_{\text{GlnB-U}}}{[\text{GlnB-U}]} \left(1 + \frac{[\text{GLN}]}{K_{\text{GLN},2}}\right)}\right] + \frac{1}{1 + \frac{K_{\text{GlnK-U}}}{[\text{GlnK-U}]} + \frac{K_{\text{GlnK-U}}}{[\text{GlnK-U}]} \left(1 + \frac{[\text{GLN}]}{K_{\text{GLN},2}}\right)}
\]
where $V$ and $K_{m}$ are the maximal enzyme rate and Michaelis constants of (de)adenylylation, $K$ are the binding affinities of GlnB(-U), GlnK(-U), and GLN to the allosteric sites of AT/AR and $n_{H}$ is the Hill-coefficient. A summary of these interactions is shown in Fig. 4.

Simulations were performed in the software MATLAB (The MathWorks, Natick, MA). An SBML format of the model is included in the Supporting Material, where we refer the reader for further details.

Model parameters: fitting and sensitivity analysis

The parameters were taken from the literature whenever possible (6 out of 21) and the rest (15 out of 21) were fitted to the 36 time points of the WT data (Table 1).

To assess the robustness of the model and to evaluate the relevance of the parameters to be fitted, we performed a global sensitivity analysis using the eFAST algorithm (37). This technique considers uncertainty in combinations of parameters and quantifies the deviation they introduce over the whole time series. See Supporting Material for details of the method and its results.

To fit the parameters of the model to the measured time series, we used the Squeeze-and-Breathe evolutionary Monte Carlo optimization algorithm (38). This algorithm minimizes a cost function $J$, which is the sum-of-squares deviation of the fractional PTM levels from the measurements, weighted by the relative errors. Mathematically, we have

$$ J(p) = \sum_{i} \sum_{j} \left[ \frac{M^{\text{mod}}}{M^{\text{total}}} - \frac{F^{\text{mod}}(p)}{F^{\text{total}}} \right] \left( \frac{M^{\text{total}}}{M^{\text{error}}} \right), $$

where $p$ denotes the vector of parameters; $M$ and $F$ denote measured and fitted, respectively; and the superscripts mod, total, and error denote total, modified, and error, respectively. The parameter values are presented in Table 1, rounded to the nearest decimal found in the confidence interval given by the distribution of optimized parameters obtained with the Squeeze-and-Breathe method (see Supporting Material for details).

RESULTS

In vivo measurements of *E. coli* temporal responses to nitrogen starvation and upshift

We measured concentrations of relevant metabolites ($\alpha$-KG and GLN) and active/inactive PTM states of the proteins GlnB, GlnK, and GS in response to dynamic variations in external ammonium (see Materials and Methods).
We use this experimental approach to measure PTM states (26,27) to link metabolic status and regulatory mechanisms.

Three E. coli cultures (a WT strain and two isogenic strains with deleted glnK or glnB) were inoculated into minimal media with a (limiting) concentration of 3 mM ammonium (see Materials and Methods). The growing cultures depleted the external nitrogen levels during the run-out period eventually leading to the starvation period measured from the point when growth stopped and extending for 40 min (Fig. 2). The starvation period was followed by a sudden 3 mM ammonium upshift to investigate the shock response (0–40 min). We sampled the cultures at specific external ammonium concentrations during run-out and at specific time points during starvation and upshift, and measured the metabolite and protein concentrations. The corresponding time courses are plotted on Fig. 3.

**In vivo regulation of GS by GlnK**

First, we investigated whether our experiments provide evidence for GlnK controlling the level of GS expression. We found no discernible difference in total GS level between ΔglnK and WT (Fig. 3), indicating that GlnK is redundant to regulate GS expression in the WT. In addition, we found that GlnK and GS were twofold overexpressed in ΔglnB (Fig. 3). This observation provides an in vivo quantification of the reduced regulatory effect of GlnK on GS expression, which has been previously evidenced in genetic studies (14).

Next, we asked whether GlnK plays a relevant role as a regulator of GS adenylylation. The response of the ΔglnB strain to external ammonium variations was consistent with GlnK substituting for GlnB in its role to control AT/AR (18). Although the growth of ΔglnB was slower than the WT during ammonium run-out, it was comparable to ΔglnK (Fig. 2), indicating that, relatively speaking, ammonium uptake was not limiting. We further found that GS was abruptly adenylylated upon nitrogen upshift in all strains (Fig. 5, c, e, and g), including the ΔglnB mutant, despite higher GS levels in the latter (Fig. 3). This suggests that, after starvation, GlnK is a potent activator of GS adenylylation. In contrast, GS was not fully deadenylylated in ΔglnB (Fig. 5 e; Fig. S6 a) under ammonium-rich conditions (unlike in WT and in ΔglnK; see Fig. 5, c and e), showing that GlnK might be less efficient in activating the AR activity. Indeed, GlnK was almost fully uridylylated (>95%) during starvation (see Fig. S6 c), consistent with the dominant GlnK species under starvation being the fully uridylylated GlnK trimer, GlnK3-U3, which is known to be a poor activator of deadenylylation in vitro (39).

Unlike in ΔglnB, we observed no evidence of GlnK-regulated GS adenylylation in the WT during ammonium run-out and starvation, the GS-A levels being similar between the WT and ΔglnK (Fig. 5, c and g). Despite this purported redundancy, the expression and uridylylation of GlnK are already induced when ammonium levels begin to decrease (19) (Figs. 3 and 5 b). Because GlnB expression is constitutive, we find that during starvation the concentration of GlnK (12.5 μM) largely exceeds that of GlnB (3.3 μM) (Fig. 3), and similarly GlnK-U (11 μM) largely exceeds GlnB-U (2.9 μM) (Fig. 5, a and b). Thus intracellular glutamine sensing by UT/UR operates before ammonium concentration becomes suboptimal for growth.

Taken together, these findings suggest a role for GlnK to prepare for a buffered return to subsequent normal nitrogen conditions after starvation, by regulating the inactivation of GS. Our measurements show that the ΔglnK strain grows at a higher rate after ammonium upshift (Fig. 2). We hypothesize that this difference is due to additional ammonium being imported via the membrane-bound ammonium channel AmtB, which accumulates during nitrogen starvation and whose activity becomes unimpeded at low levels of GlnK.

To understand further the interaction between GlnB and GlnK during nitrogen run-out, starvation, and upshift, we constructed a mathematical model motivated by our in vivo dynamic measurements of protein (total and PTM) and metabolite concentrations. To date, the use of directly determined PTM data in models of regulation of GlnB and GlnK has been lacking, yet such modification directly determines their functionality. We now present an inclusive modeling approach to link GlnB and GlnK activity via PTMs to metabolic status and control of nitrogen assimilation processes.

**Mathematical modeling of the enzymatic network of nitrogen signaling and regulation**

In view of the experimental data, we built an ODE model to describe the dynamics of PTM states, i.e., the (de)uridylylation of GlnB and GlnK and the (de)adenylylation of GS in response to temporal inputs (drivers). An ODE model was adopted due to the large copy numbers observed—the smallest being GlnB with an average of ~10^3 molecules per cell. We based our equations on the enzyme mechanisms reported in the literature with the aim of a parsimonious model, only including terms with an observable effect in our experiments. The resulting model remains mechanistic with a moderate number of parameters, facilitating direct comparison to experiments and parameter fitting.

The terms of the ODE model are derived from the biochemical details of competition for the active and allosteric sites, which is inherent to the uridylylation and adenylylation reactions, and from the formation of complexes between GlnK and AmtB. In addition, we use five measured input drives to isolate the responses pertaining to transcription and other parts of
the *E. coli* metabolism. These include concentrations of metabolites GLN and α-KG, which act as enzyme effectors and reflect the metabolic state of the cell, and the total concentrations of GlnB, GlnK, and GS, which reflect the relevant transcriptional responses of the cell (Fig. 3). We further assume that key cofactors (e.g., ATP, NADPH) remain at homeostasis under our experimental conditions (10), so that their concentrations can be approximated to be constant and can thus be absorbed into the kinetic parameters of the equations.

The model parameters include binding affinities (Kₐ) of various effectors to active and allosteric sites of the enzymes, Michaelis constants (Kₘ), maximum enzyme rates (Vₘₐₓ), and parameters representing AmtB-GlnK complex formation (Table 1). Whenever possible, we used parameters from the biochemical literature, and we fitted the rest to the WT experimental time-courses using the Squeeze-and-Breathe algorithm (38). To confirm that the parameters capture meaningfully the experimental observations, we also performed a global sensitivity analysis over the time series (37). For details, see Materials and Methods and the Supporting Material.

To make predictions for the ΔglnB and ΔglnK mutants, we set the corresponding reaction rates to zero, fixing all other parameters at values fitted to the WT time-course data. We then generate predicted time series for the PTM protein states under the experimentally measured drives. These predictions are compared to the independently obtained measurements.

**Modeling the mechanism of GlnB and GlnK uridylylation**

The bifunctional enzyme UT/UR has two independent active sites catalyzing uridylylation (UT) and deuridylylation (UR), which are highly specific for GlnB and GlnB-U, respectively (31); it also has an allosteric site for glutamine (Fig. 4a). Due to the similarity between GlnB and GlnK, we assume similar specificity of UT/UR active sites to GlnK/GlnK-U, yet with different binding affinities. Hence we model GlnB and GlnK uridylylation as two monocycles, GlnB-UT/UR and GlnK-UT/UR, which operate in parallel but not independently, because the total amount of enzyme is distributed between them at any given time. We further consider that the binding of glutamine inhibits the uridylylation of GlnB/GlnK and activates the deuridylylation of GlnB-U/GlnK-U (8) (Eq. 2; Materials and Methods).

As shown in Fig. 5a, our model captures accurately the excitatory and inhibitory effects in the measured GlnB uridylylation under different conditions in the WT without the need for modeling ternary complexes explicitly as in the more complex model in Straube (12), (Fig. S5). The parameters fitted to the WT data show that the affinities of GlnK and GlnK-U to AT/AR (Kₐ = 9.9 and 59.8 μM, respectively) are significantly lower than those of GlnB and GlnB-U (Kₐ = 3 and 2 μM, respectively), which are known experimentally (11). Hence GlnK only affects nitrogen assimilation when its concentration is several times higher than GlnB, in agreement with previous in vitro findings (14).

Although this model allows us to fit well the overall WT time measurements, it cannot capture the GlnK-U level in response to the ammonium upshift after starvation (Fig. 5a). Moreover, the model overpredicts the level of GlnK-U in the ΔglnB knock-out (Fig. 5b). In the next section we discuss an additional mechanism, which is
necessary to make accurate predictions of the observed GlnK-U levels.

**Sequestration of GlnK is necessary to predict uridylylation levels**

To accurately describe GlnK uridylylation dynamics, we take into account the interaction of GlnK with AmtB. The membrane-bound channel protein AmtB facilitates ammonium active import to the cell. AmtB channels are blocked when AmtB forms a complex with trimers of deuridylylated GlnK above 20–50 μM external ammonium concentrations (16). Hence AmtB-facilitated transport is negligible in our experiments before complete run-out. However, the formation of complexes between AmtB and GlnK does affect the dynamical responses, because it provides a mechanism

| TABLE 1 Model Parameters |
|---------------------------|
|                          | UT/UR | AT/AR |
| Maximum enzyme rates     |       |       |
| V<sub>UT</sub>           | —     | 976.9 μM/min |
| V<sub>UR</sub>           | —     | 473.4 μM/min |
| Michaelis-Menten constants |     |       |
| K<sub>m,GlnB</sub>       | 3 μM  | 133.8 μM |
| K<sub>m,GlnB-U</sub>     | 2 μM  | 56.1 μM |
| K<sub>m,GlnK</sub>       | —     | 9.9 μM |
| K<sub>m,GlnK-U</sub>     | —     | 59.8 μM |
| Dissociation constants   |       |       |
| K<sub>GLN,1</sub>        | 90 μM | —     |
| K<sub>α-KGL,1</sub>      | —     | 3.0 mM |
| K<sub>GLN,2</sub>        | —     | 15.0 μM |
| K<sub>GLN,2-A</sub>      | —     | 0.25 μM |
| K<sub>α-KGL,2</sub>      | —     | —     |
| K<sub>GlnB</sub>         | —     | 8.3 μM |
| K<sub>GlnK</sub>         | —     | 9.7 μM |
| K<sub>GlnK-U</sub>       | —     | 1.4 mM |
| K<sub>GlnK</sub>         | —     | 0.89 mM |
| K<sub>GlnK-U</sub>       | —     | —     |
| Hill coefficients        |       |       |
| n<sub>UT</sub>           | 3 (17)| —     |
| Fractional sequestration | x     | 0.4   |

![Model fitted to data](image)

**FIGURE 5** Time responses of PTM protein levels in the WT and two knock-out mutants. (a) Time responses of GlnB uridylylation, GlnK uridylylation, and GS adenylylation in the WT strain (experimental measurements and fitted model, with and without sequestration). (b) and (c) Experimental measurements of GlnB uridylylation, GlnK uridylylation, and GS adenylylation for knock-outs: (b) ΔglnB and (c) ΔglnK, compared in both cases to the dynamics predicted by our model fitted only to the WT data. The symbols and error bars represent measured average protein concentrations mean ± SE (n = 3). The lines correspond to fits and prediction of our model, as indicated. The gray-shaded area marks the starvation period. The model with sequestration provides a significantly better fit according to information criteria for model selection (see text).
for the sequestration of GlnK and GlnK-U at the membrane (40). Note that whereas fully uridylylated trimers cannot bind AmtB (15), our measurements show that the uridylylation level of GlnK is ~30% after starvation (see Fig. S6 c), suggesting that the GlnK trimers will be mostly monouridylylated, i.e., one uridylylated GlnK per GlnK trimer, on average. In our model, we assume that both fully uridylylated GlnK trimers and partially uridylylated GlnK trimers may be functionally sequestered to the membrane. However, unlike the fully uridylylated GlnK trimers, partially uridylylated GlnK trimers do not block AmtB channel activity.

We model AmtB-GlnK complex formation by allowing a proportion of the total GlnK to be sequestered with a Hill-function dependence (Eq. 4; Materials and Methods) on the concentration of α-KG (16). Note that, because high levels of α-KG level promote the dissociation of the AmtB-GlnK complex, sequestration only occurs during external ammonium abundance, i.e., when the α-KG levels are low (Fig. 3).

The model with sequestration fitted to the WT data is able to capture the GlnK-U levels after nitrogen upshift (Fig. 5 a). To justify the necessity of the two additional parameters (Kα-KG1, x) involved in GlnK sequestration, we use the fitted model to predict the uridylylation states of GlnK and GlnB in the ΔglnK and ΔglnB knock-outs, and compare them to the measured time-courses (Fig. 5, b and c). This approach has been used before to develop systems biology models (41,42). Our predictions agree with the measurements: without sequestration, the model overpredicts the levels of GlnK-U before starvation (time before ~40 min) and after nitrogen upshift (time after 0 min) in the ΔglnB mutant (Fig. 5 d). To quantify this, we compute the error of both models (with and without sequestration) against the data (7), and rank both models according to two information theoretic criteria (AICc, BIC), which penalize the additional parameter complexity against any improvement in the error of the model. The extended model with sequestration is clearly selected by both information criteria (see Table S2) lending further basis for the need for a GlnK sequestration term during nitrogen excess.

The higher growth rate observed in the ΔglnK strain after starvation (Fig. 2) is also consistent with GlnK sequestration. Because amtB is still present in this strain, AmtB is expected to accumulate during nitrogen starvation, which provides unrestricted ammonium import and higher growth rate in the short term.

**GlnK can regulate AT/AR in the absence of GlnB**

Our results so far indicate that GlnK not only competes with GlnB as a substrate or UT/UR, but also provides a link between active membrane transport and carbon metabolism through the interaction with α-KG. To further test this mechanism, we asked: is GlnK sufficient on its own to regulate the adenylylation enzyme AT/AR in the absence of GlnB? If so, one would expect that the predicted GlnK-U levels in the ΔglnB strain should account correctly for GS-A levels and, hence, for the activity of GS in nitrogen assimilation.

To test this hypothesis, we extended our model to include GS adenyllylation. Similarly to UT/UR, the two antagonistic activities of AT/AR are modeled as independent unidirectional reactions, justified by structural studies showing the two active sites to be well separated (33), making interaction between the AT and AR domains less likely (Fig. 4 b).

We model different facets of AT/AR regulation as found in the literature (Fig. 4 b). First, AT and AR activities are inhibited by the products, GS-A and GS, respectively (7). Second, in the absence of allosteric effectors, AT/AR has no observable activity (7). From this state, the rates of AT and AR activities are regulated by five allosteric effectors, which do not affect the binding rates of substrates (21). In particular, GLN, GlnB, and GlnB-U may bind to three distinct sites (7,21,33). As above, we assume that GlnK(-U) has the same specificity as GlnB(-U) but different affinity, so that GlnB and GlnK compete for one allosteric site, and GlnB-U and GlnK-U compete for the other. Finally, to account for intramolecular signaling (33), we allow the activation parameters of GlnB, GlnB-U, GlnK, and GlnK-U to depend on α-KG (Eq. 5; Materials and Methods). We encapsulate these terms into the reaction schemes (Eq. 6) by generalizing the classical allosteric activation model (43) for two competing effectors (see Supporting Material for details).

The additional equation for GS-A was fitted to the WT data and captures well the observed variability (Fig. 5 a). To avoid overfitting, we keep fixed all parameters related to UT/UR and sequestration, and fix the insensitive activation parameters Kα-KG and Kα-KG-U to the values reported by Jiang et al. (7) (Table 1; Materials and Methods; Supporting Material). In contrast, the activation parameters Kα-KG and Kα-KG-U are relatively insensitive in the WT, yet essential to predict GS-A levels in the ΔglnB strain. The fitted activation constant KGLN,2 for AT/AR is in the range reported in Jiang et al. (7) and the Hill coefficient nAT is found to be as reported in Mutalik et al. (35). Note also that the activation constants of GlnK and GlnK-U for AT/AR are much higher than those of GlnB and GlnB-U, consistent with their observed lower affinity (14).

To assess the model fitted to the WT data, we predict the level of GS-A for the two knock-outs in response to the measured drives. The predicted responses agree with the measured GS-A levels in both strains (Fig. 5, b and c). The GlnB-deficient strain (ΔglnB) is able to regulate GS activity in response to external changes in ammonium. The prediction for the ΔglnB strain underestimates the GS-A level before starvation—we consider the possible source for this discrepancy in the Discussion. Given that GS regulation depends on the fine balance between GlnB/GlnB-U and GlnK/GlnK-U together with the level of GLN and...
DISCUSSION

We have investigated the role of GlnK in the dynamic regulation of ammonium assimilation from a systems perspective, and have argued that paradoxical observations about GlnK stem from the subtle interplay of regulatory mechanisms on two levels: transcriptional and posttranslational. To decouple both levels of regulation, we collected concurrent in vivo time-courses of metabolite, total protein, and PTM protein concentrations in response to time-varying external ammonium levels. We analyzed the data in conjunction with a mechanistic model derived from biochemical principles. The combined analysis allowed us to fit the WT dynamics of PTMs, and to use the fitted model to predict the dynamic responses of experimental data from genetic knock-outs, shedding light on experimental ambiguities about the regulatory role of GlnK.

We found that competition between GlnB and GlnK for the bifunctional enzyme UT/UR together with GlnK sequestration by AmtB describe the uridylylation responses in the WT and can predict the response of two mutants under dynamic ammonium perturbations. AmtB-GlnK complex formation not only blocks ammonium import (16), but also rapidly sequesters GlnK, whereas the less abundant GlnK limits ammonium assimilation by facilitating more rapid deuridylylation of GlnK-U (Fig. 5), and thus, higher GS-A levels. Thus GlnK dampens the assimilatory response to ammonium upshift, perhaps to avoid excess ammonium uptake causing the depletion of the glutamate pool (4,5). The fact that sequestration is regulated by α-KG (a product of the carbon metabolism), suggests that nitrogen shock responses could also help to avoid untoward impacts on carbon status.

Our experiments showed that during ammonium-rich conditions, GlnK is present at low level and does not influence GS production and adenylylation, which is instead regulated by the more potent GlnB. However, due to the induction of glnK during ammonium run-out, GlnK outnumbers GlnB fourfold during starvation (Fig. 3). To examine the capability of GlnK for AT/AR regulation after ammonium upshift, we developed a mathematical model of GS adenylylation based on allosteric competition between GlnB and GlnK for AT/AR. The model predicts accurately the abrupt increase in GS-A levels after ammonium upshift in both the ΔglnB and ΔglnK strains (Fig. 5) showing that GlnB and GlnK are each independently sufficient for effective AT/AR regulation. Our model slightly underestimates the GS-A levels before starvation in the ΔglnB strain. Because the model was fitted to the WT, where both GlnB and GlnK are present, this mismatch may indicate unaccounted-for interactions that are disrupted when deleting the glnB gene, e.g., GlnB and GlnK forming heterotrimers (39,44,45).

To check the relevance of GlnK regulation of AT/AR, we used our model to simulate two in silico cellular scenarios. To begin, we considered our model for a computational strain where GlnK does not interact with AT/AR (by setting $K_{\text{GlnK}} \gg [\text{GlnK}]$ and $K_{\text{GlnK-U}} \gg [\text{GlnK-U}]$, such that the terms involving GlnK and GlnK-U drop out in Eq. 6), and hence AT/AR is regulated only by GlnB. In this scenario where the regulatory role of GlnK is removed, the predicted GS-A levels in response to ammonium upshift after starvation are reduced (Fig. 6a), thus leading to an increase in GS activity and larger ammonium assimilation. This is consistent with the proposed role of GlnK as a buffer to ammonium shock, through the adenylylation (inactivation)
of GS. Noting that the level of GS-A does not change during run-out and starvation, we also used our model to predict the response of another computational strain (Fig. 6 b) where the expression of glnK is constitutive and unregulated (by fixing [GlnK_{total}] as a constant). In this scenario, if GlnK abundance is kept fixed at the late-starved level (26 μM), GS-A levels remain elevated during run-out and starvation. This simulation supports the notion that GlnK must be kept downregulated during nitrogen abundance, because early glnK expression would lead to reduced ammonium assimilation due to increased GS-A levels. During ammonium run-out and starvation, amtB (and conjointly glnK, being on the same operon) is expressed to increase ammonium uptake via AmtB channels. The resulting higher levels of GlnK induced by starvation serve also to control potential overshoots in ammonium levels after starvation not only by blocking AmtB channels, but also by directly reducing GS activity through adenylylation.

Beyond nitrogen regulation, our work exemplifies the need for in vivo experimental time series data in developing predictive models. Time-course inputs together with classic genetic knock-outs provide tools to gain insight into the dynamic aspects of regulation in signaling pathways. Although large-scale biochemical models can be powerful, their applicability is many times hampered due to the large number of unknown parameters they contain, which need to be fitted to scarce data. Here we derived a small set of mathematical modules commensurate with the observed dynamics, and justified their relevance by a global parameter sensitivity analysis. We used a recently developed parameter fitting algorithm (38), which is especially appropriate for time-courses, to fit the WT data, and we then used the fitted model to predict out-of-sample dynamical observations from the genetic knock-outs.

Although we have focused here on Escherichia coli, with the dual GlnB/GlnK proteins, we expect nitrogen assimilation and transport to be more strongly coupled in bacteria containing only one GlnB-like protein (e.g., cyanobacteria, Azotobacter), enabling the tight coordination of carbon and nitrogen metabolisms. Similarly, patterns of sequestration may be a biophysical regulatory mechanism operating widely in other contexts, and understanding its spatiotemporal dynamics in the cell would help link gene and metabolic regulation responses to biophysical feedback to environmental inputs (46).

SUPPORTING MATERIAL

Supporting Materials and Methods, seven figures, and two tables are available at http://www.biophysj.org/biophysj/supplemental/S0006-3495(17)30428-9.

AUTHOR CONTRIBUTIONS

A.G., M. Barahona, M. Buck, and J.S. designed the study. A.G. performed the analysis under the supervision of M. Barahona and M. Buck. J.S. designed and coordinated experiments. V.B., J.G.B., F.H., and M.H.B. performed the experiments. A.G., M. Barahona, J.S., and M. Buck wrote the manuscript, with inputs from other authors.

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