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Low-Threshold and Wavelength-Tunable InGaN Tubular WGM Laser Embedded in a Flexible Substrate

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Abstract: We have fabricated a tubular whispering gallery mode laser based on InGaN/GaN quantum wells and transferred it onto a flexible substrate. Compared with those without the transferring processes, the threshold energy density was reduced by 60%, at about 25.55 μJ/cm², while a high-quality factor of >15,000 was obtained. Finite-difference time-domain simulation demonstrated that such a low threshold energy density can be attributed to the decreased mode volume, from 1.32 × 10⁻³ μm³ to 6.92 × 10⁻⁴ μm³. The wavelength dependences on strain were found to be 5.83 nm, 1.38 nm, and 2.39 nm per stretching unit c in the X, Y, and Z directions, respectively. Such strain sensitivity was attributed to the deformation of the GaN microtube and the change in the refractive index of the PDMS.

Keywords: WGM; microtube; cavity

1. Introduction

In recent years, electronic/photonics components integrated on stretchable substrates have created enormous research interests due to their wide and novel applications in soft robots [1,2], bioelectric medicine [3,4], human augmentation [5], displays [6,7], energy storage devices [8,9], and wearable sensing [10–12]. Among them, micro/nano lasers embedded on a stretchable substrate have been widely studied as random laser sources [13–16], strain sensors [17,18], and for other applications, because they can avoid rigid material substrates and render their applications in a deformable state or as soft systems. Strain sensors with a high detection sensitivity, which are used to monitor small-scale deformations, call for a small device footprint, high-power consumption, and narrow linewidth. Meanwhile, whispering gallery mode (WGM) lasers, known for their small mode volume and high quality factors (Q), are excellent optical cavities for low threshold micro/nano laser with narrow linewidths [19]. Due to the excellent optoelectronic properties, such as a wide wavelength, strong light–matter interaction, stable physical and chemical properties, gallium nitride (GaN)-based materials have been used as a gain material for WGM resonators [20]. Thanks to the development of electrochemical etching [21] and photoelectrochemical etching [22], ultra-thin GaN film has been demonstrated using chemical exfoliation in previous works [23–25], which makes gallium nitride microtube lasers possible. Previous studies of WGM lasers employed microdisks or microfiber embedded in a flexible substrate [26–30] as strain sensors. For example, a GaN microdisk laser with a diameter of 1.2 μm embedded in a polydimethylsiloxane (PDMS) substrate as a strain sensor has a blue-shift per stretching unit of about 4.0 nm [29]. In addition, by applying different forms of strain to a polymer microfiber in the flexible PDMS substrate, bi-directional tuning of the wavelength was achieved [27]. However, only a relatively low strain response was achieved due to the small refractive index variations of the flexible substrate materials. Meanwhile, the low quality factor of GaN-based microdisks usually leads to a low limit of detection (LOD). In this
study, we fabricated a three-dimensional (3D) tubular WGM microcavity and transferred it onto a flexible transparent PDMS substrate. The ultra-thin well of the tubular WGM microcavity (less than 60 nm) allows it to be easily deformed under applied force and is sensitive to three-dimensional strain. A low threshold excitation energy density was achieved while high quality factors were maintained due to the small mode volume and the large refractive index contrast between the GaN material and the PDMS substrate [31]. The unique geometry of the tubular structure has a 3D mode confinement and trimmed resonant modes, making it a strong candidate for 3D microscale strain gauges, photonic integrated circuits, flexible laser displays, or other sensors.

2. Materials and Methods

2.1. Microtubes Preparation

A 2-µm undoped GaN buffer layer was grown on a sapphire substrate followed by a 2-µm n-type GaN (3 × 10^{18} cm^{-3}) and a 150-nm highly doped n^{+}-type GaN layer (3 × 10^{19} cm^{-3}). During the subsequent electrochemical etching process, the n-GaN layer acted mainly as a current-conducting layer, and the highly doped n^{+}-GaN was etched away as the sacrificial layer. Finally, 3 pairs of 3-nm InGaN quantum well (QW)/3-nm GaN quantum barrier (QB) were grown as the gain material. The 20-nm GaN layer was followed by a 20-nm top Al_{0.25}Ga_{0.75}N that were finally grown as the stress-generating layers. A rectangular (50 × 25 µm²) pattern was prepared using traditional photolithography and inductively coupled plasma (ICP) etching techniques. Then, electrochemical etching was used for the removal of the sacrificial layer to release the gain material and the stress-generating layers. Due to the lattice mismatch between the stress-generating layers, self-rolling occurred when the sacrificial layer was removed and microtubes were formed. A more detailed process can be found in our previous work [32,33].

2.2. Transfer Process

To obtain a flexible platform, it was decided to lift the microtubes from the native GaN-doped layer to a foreign flexible substrate. A 300-µm-thin PDMS film was first deposited on a glass substrate via spin coating and was then baked at 90 °C for 10 min. The GaN wafer was put on the thin PDMS film with the sapphire substrate facing up. The GaN microcavity adhered to the soft PDMS and the microtube was transferred to the PDMS by mechanically lifting it off the wafer. Finally, another thin PDMS film of about 50 µm in thickness was spun on the GaN microtubes for protection and mechanical support purposes. Optical microscopy images of the GaN microtubes on sapphire and PDMS substrates are shown in Figure 1a,b, respectively, which indicates that the GaN microtubes were successfully peeled off of the n-GaN layer and sapphire. Figure 1c shows a side view of a single 5-µm diameter microtube with a good morphology and smooth surface. The wall thickness of the microtube was about 57 nm.

Figure 1. Optical images of (a) arrays of microtubes on GaN layers and (b) arrays of microtubes in PDMS film. (c) Side view of SEM image of microtubes with 57-nm wall thickness.
2.3. Measurement Setup

Figure 2a shows a schematic diagram of experimental setup for the strain test in the X and Z directions. The microtube embedded in the flexible PDMS substrate was fixed on a micrometer table, through which we could adjust the magnitude, as well as the direction, of the force. To test the strain in the Y direction, the flexible substrate was fixed to the center of two pieces of glass, as shown in Figure 2b. By applying force to the glass in the vertical direction, compressive strain could be generated in the microtubes. Spectra of the GaN microtubes were collected in a micro-photoluminescence (PL) setup, in which an objective lens served the function of optical excitation, as well as PL signal collection. A 355-nm diode laser with a 350-ps pulse time and 1000 Hz pulse frequency was used as the excitation source at room temperature. The laser spot could be focused down to a diameter of 20 µm on the surface of the microtube.

3. Results and Discussion

Figure 3a shows the PL spectra of a microtube in PDMS, which was excited from 24.5 µJ/cm² to 27.0 µJ/cm². All spectra correspond to the TM polarization mode due to the fact that the TE mode was not sustainable for such thin-walled microcavities [32]. The optical mode separation (free spectral range (FSR)) was measured at around 4.0 nm when λ was 430 nm, which matched the calculations using the periodic boundary condition 2πneffR = mλ. In this equation, R represents the radius of the microtubule, λ represents the wavelength of the laser, neff represents the effective refractive index of the microtube material, and m represents the azimuthal mode number. As shown in Figure 3a we also found a series of resonant peaks at 419.03, 422.95, 426.79, 430.82, 435.07, 439.38 nm, etc., which correspond to successive azimuthal modes. As the pump energy increased, certain resonance modes, such at 426.79 nm and 430.82 nm, changed from spontaneous emission to stimulated emission. Figure 3b shows the PL intensity and full width at half maximum (FWHM) versus pump energy density for the 426.79-nm peak of the microtube in the PDMS substrate. When the threshold was reached, the linewidth of the resonance peak decreased from 0.29 nm to 0.07 nm, confirming the occurrence of stimulated emission. Figure 3c shows the PL spectrum of another microtube with a narrow FWHM of about 19.8 pm and 24.1 pm at 427.25 nm and 429.89 nm, and the corresponding Q factors are 21,578 and 17,837, respectively. Such numbers were considered large enough compared to other Q values of tubular microcavity that were reported previously [34–36]. Figure 3d shows a box-plot showing a comparison of the threshold and the Q factor between the PDMS and GaN substrates. To eliminate the individual difference, five microtubes were measured. The average threshold was reduced from 62.86 µJ/cm² to 27.34 µJ/cm² while the Q value fluctuated in a relatively large range, resulting in no significant difference before and after the transfer.
The Purcell effect describes the enhancement of spontaneous emission rate by the environment. In most cases, one can reduce the mode volume of a microcavity to lower the excitation threshold, which will also lead to an increase in the Purcell factor [37]. The effective mode volume of a microcavity is equal to the total electric field energy in the microcavity divided by the maximum electric field energy density. In addition to absorption by the GaN material and curvature-induced light scattering, light leakage through n-doped GaN and sapphire substrates also leads to an increase in the mode volume of the microcavity. When the pump energy was above the threshold, there was no obvious difference in the Q-factor of the GaN microtubes, with or without the transfer process. Thus, the threshold change is more likely caused by the changing of the mode volume. The mode volume was investigated using finite-different time-domain (FDTD) simulations with an embedded modal volume analysis tool for the confined mode. The GaN refractive index at 450 nm was set to be 2.4 while that of PDMS was set as 1.41.

Figure 4a,b shows the electric field distribution inside the microtube embedded in the PDMS substrate, as well as on the GaN substrate, respectively. The amplitude of the electrical field intensity was indicated by the color bar. As the Figure 4a shows, light from the gain material (QWs) is limited by total internal reflection between the outer interface of GaN/PDMS and the inner interface of GaN/air. The mode volume of the microtube with GaN substrate was calculated to be $\sim 1.32 \times 10^{-3} \, \mu m^3$ by FDTD simulation while that of the microtube embedded in the PDMS substrate is $\sim 6.92 \times 10^{-4} \, \mu m^3$. The reduction of the mode volume caused the laser threshold to decrease from 62.86 $\mu J/cm^2$ to 27.34 $\mu J/cm^2$. From Figure 4b, one can see that light leaks through the GaN substrate underneath the microtube due to the lack of refractive index contrast. The proportional energy that leaked through the GaN layer substrate was as high as 11.03% of the total energy propagating in the system. The proportional energy that leaked through the PDMS substrate was about 1.21%. This was caused by the excessive refractive index difference between the PDMS layer and the GaN microtube.
The measured PL spectra under stretching conditions in the Z direction are described in Figure 5a, in which the Z direction is defined as the axial direction while the cross section of the microtube is set in the X–Y plane. The geometrical deformation of the PDMS can be described as stretching unit $\varepsilon$, which was defined as $\Delta d/d$ to describe the percentage change of the dimension. Parameter $d$ is the original length of the substrate and $\Delta d$ represents the deformation length under tensile forces. The wavelength shift as a function of stretching unit $\varepsilon$ in Z direction is plotted in Figure 5b while that of the X and Y directions are shown in Figure 5c,d, respectively. We used the PL blue-shift per stretching unit as the detection sensitivity of the microtube strain sensor. The PL blue-shifts of the microtube are about 5.83, 1.38, and 2.39 nm per stretching unit in the X, Y, and Z directions, respectively. Simulation using FDTD (not shown) demonstrated that, as the strain on the PDMS substrate increased from 0 to 0.1, the OPSR of the laser emission decreased from 10.26 dB to 1.01 dB. According to the periodic boundary condition, the blue-shift was attributed to the change in the index of the surrounding PDMS material under different tensile stresses while the red-shift occurred under compressive strain [27,29]. However, in our work, both the tensile stress and compressive strain conditions led to a blue-shift. Thus, the deformation of micro-cavity should have played a role to counter balance in one way or another. Therefore, it is necessary to study how the deformation of a microcavity and the refractive index changes of PDMS affect the microtube wavelength shift all together from a system point of view. The structural deformations of the microcavity under strain were investigated by establishing a simulation model using finite-element analysis (FEA) software.

Figure 6(a1) shows the 3D deformation distribution under 0.05 $\varepsilon$ tensile strain from the Z direction as if the microtube was stretched from the right end while fixing the left end. The cross-sectional deformation magnitude of the X and Y components are shown in Figure 6(a2,a3), respectively. The direction and the length of the arrow represent the direction and the magnitude of the deformation. The calculations show that the perimeter length (L) of the microtube decreases as the tensile strain increases. The changed length ($\Delta L$) can be calculated by: $\Delta L = L\Delta\varepsilon/\lambda$ where $\Delta\varepsilon$ represents the blue-shift. Figure 6c shows the numerical simulation results of the microtubule circumference variations with applied strain. The $\Delta L$ in the Z direction was calculated and the corresponding to the per stretching unit was 0.09 nm. In the same way, we could simulate the deformation distribution under 0.05 $\varepsilon$ tensile strain, as if the microtube was pressed from the top while fixing the bottom (Figure 6(b1)). The cross-sectional deformation magnitude of the X component and Y component are show in Figure 6(b2,b3), respectively. Due to the rotational symmetry in the X–Y plane blue-shift per stretching unit by strain in the both X and Y direction show the same value of 4.60 nm/$\varepsilon$ while the value in the Z direction is 0.09 nm/$\varepsilon$. Blue-shift per
stretching unit in the X, Y, and Z directions were measured as 5.83, 1.38 and 2.39 nm/\(\varepsilon\), respectively. The discrepancy between the calculations and measurements can be attributed to the refractive index change of the PDMS alone. The variation introduced by the PDMS could be estimated as 2.23 nm/\(\varepsilon\) ((5.83 nm/\(\varepsilon\) − 1.38 nm/\(\varepsilon\))/2), meaning that when PDMS stretched one unit of strain, the change in the refractive index will lead to a blue-shift of 2.23 nm/\(\varepsilon\). The measured blue-shift with an applied force in the Z direction should be attributed to both the index change of the PDMS and the deformation of the microtube. The total per stretching unit in the simulation was about 2.32 nm/\(\varepsilon\) (2.23 nm/\(\varepsilon\) from PDMS and 0.09 nm/\(\varepsilon\) from microtube), which was very close to the experimental result of 2.39 nm/\(\varepsilon\).

Presently, we proved that the stress-induced blue-shift was caused by deformation of both the microtube and the PDMS. This helps us to better design and characterize a strain sensor with an ultra-thin microtube cavity in a flexible substrate.

**Figure 5.** (a) PL spectra in the Z direction measured under different stretching conditions from 0 to 0.09 \(\varepsilon\). (b-d) show the measured lasing wavelength changing under various tensile conditions in the Z and X directions and compressive conditions in the Y direction, respectively. The insets in (b-d) show the direction of applied force.

**Figure 6.** (a1) The 3D deformation distribution under 0.05 \(\varepsilon\) tensile strain from the Z direction. (a2,a3) the cross-sectional deformation magnitude of the X component and the Y component, respectively. (b1) The 3D deformation distribution under −0.05 \(\varepsilon\) compressive strain from the Z direction. (b2,b3) the cross-sectional deformation magnitude of the X component and the Y components, respectively. (c) Simulated microtubule circumference variation as a function of applied strain.
4. Conclusions

In summary, a blue QW-based ultra-thin WGM microtube cavity was fabricated and successfully transferred to a PDMS matrix. The removal of the native GaN substrate and the ultra-thin wall thickness enabled a reduced mode volume. This leads to a smaller threshold of 25.55 µl/cm² while a high-quality factor of >15,000 was obtained compared to that before the transfer. By comparing the measured and simulated results, we found that the strain sensitivity was, not only affected by the deformation of the microtube, but also affected by the refractive index change caused by PDMS deformation. Both effects are suggested to be carefully considered in strain sensor design and characterization. This tunable low-threshold tubular microcavity hold, protected by the PDMS, may help to realize small mode volume light sources that are needed in advanced strain sensors for multiple purposes and complex environments.

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