Multimodal Emotion Recognition Using Non-Inertial Loss Function

Jargalsaikhan Orgil\textsuperscript{1}, Stephen Karungaru\textsuperscript{1}, Kenji Terada\textsuperscript{1} and Ganbold Shagdar\textsuperscript{2}

\textsuperscript{1}Graduate School of Technology, Industrial and Social Sciences, Tokushima University, Tokushima 770-0851, Japan
\textsuperscript{2}Graduate School of Information and Communication Technology, Mongolian University of Science Technology
Ulaanbaatar 770-0851, Mongolia
E-mail: orgil@must.edu.mn, karungaru@tokushima-u.ac.jp

Abstract Automatic understanding of human emotion in a wild setting using audiovisual signals is extremely challenging. Latent continuous dimensions can be used to accomplish the analysis of human emotional states, behaviors, and reactions displayed in real-world settings. Moreover, Valence and Arousal combinations constitute well-known and effective representations of emotions. In this paper, a new Non-inertial loss function is proposed to train emotion recognition deep learning models. It is evaluated in wild settings using four types of candidate networks with different pipelines and sequence lengths. It is then compared to the Concordance Correlation Coefficient (CCC) and Mean Squared Error (MSE) losses commonly used for training. To prove its effectiveness on efficiency and stability in continuous or non-continuous input data, experiments were performed using the Aff-Wild dataset. Encouraging results were obtained.

Keywords: deep emotion recognition, emotion recognition, emotion, body language, intonation

1. Introduction

To understand each other, emotions have played an important predictive role. Emotions are an extremely complex brain function that reacts to previous actions based on the human brain functional system, called the “Limbic System”. Recently, there has been an enormous interest in this emotion recognition field.

Emotion can be recognized using many methods including voice intonation, body pose, and more complex ones such as electroencephalography (EEG) \cite{1}, etc. Facial emotion can be visualized by the expansion and contraction of the muscles located around the mouth, nose, and eyes \cite{6}. Previous studies of facial emotion recognition concentrated on seven basic categories: anger, fear, disgust, happiness, sadness, surprise, and contempt \cite{5}. Moreover, Action Units (AUs) \cite{2}, \cite{3}, \cite{4} were proposed to model facial behavior, and the combination of AUs could also be utilized for facial expression recognition. Most studies are based on the seven basic categories \cite{7}, \cite{8}, \cite{9}, \cite{10}, \cite{11}, \cite{12} with some researchers using triplet expression recognition \cite{13}.

Consequently, facial expression recognition has attracted renewed attention owing to recent advanced network architectures. In facial expression recognition, real-time automated analysis of facial expression in video plays an essential role in implementing human-computer interaction interfaces.

The 2-D Emotion Wheel \cite{22}, shows valence ranging from extremely positive to negative and arousal ranging from extremely active to passive. Based on the data from the activity a person is engaged in, discriminating information on the valence of a person’s emotions may be known. Emotion sensing parameters can be distinguished as to whether they provide information on qualification of the valence aspect or the arousal aspect. There are many related works in this field depending on data sets used and models proposed \cite{20}, \cite{21}. There are also previous studies on emotion recognition in videos \cite{18}, \cite{25}. Valence and Arousal (V-A) are not separated values; binding these two parameters describe an emotion.

For most emotion recognition methods so far, the Concordance Correlation Coefficient (CCC) loss and the Mean Squared Error (MSE) loss are widely used during training. FATAUVA-Net Chang et al. \cite{25} has provided the best-confirmed results using mean CCC and mean MSE for valence and arousal. The authors concentrated on the connection between V-A estimation and Action Unit such as the face and its parts. Moreover, their research environment was based on a
wild setting. Yang et al. [15] concentrated on feature extraction. A network was assembled that extracted features with a Recurrent unit and was trained on MSE loss. Vielzeuf et al. [14] trained audiovisual ensemble network on emotion video classification. Mi-MAMO Net Deng et al. [18] trained a spatial, temporal network with CCC loss.

Two criteria were measured for evaluating the performance of the networks; Valence and Arousal fractional range is between $[-1, 1]$. The main problem is that no loss function that can quickly train a given network on less data. Moreover, Valence and Arousal are not separated values, and it is usually considered important to train them together in a coordinate system points.

Therefore, in this paper, the unit circle map of the V-A is used. Annotated targets are moving objects in the unit circle map of Valence and Arousal. Predictions of the model should be the small difference value of targets. Moreover, there are 3 dynamical physical calculation formulas used in the proposed method. This is the basis of the proposed loss function that we call "Non-Inertial". Experiments were conducted on multiple model architectures and sequence lengths in training.

The contributions of the proposed method are as follows:

1. The new loss function allows for Valence and Arousal to be viewed together
2. Ability to train on less data
3. Better results
4. Faster training times

As shown in Table 1, emotion recognition model input parameters can be linked to whether they provide the Valence or Arousal aspect quantification information [27]. This research uses the following relations: Facial expression, facial muscle activity around the lip, eye, and nose, voice, and intonation. Body pose relation is not engaged.

| Emotion-related effect       | Arousal | Valence |
|-----------------------------|---------|---------|
| Emotion induced sweating    | +       | +       |
| Breathing rhythm variations | +       | +       |
| Heart rate variability      | +       | +       |
| Blood pressure              | +       |         |
| Core body temperature       | +       |         |
| Heart rate                  | +       |         |
| Facial expression           |         | +       |
| Facial muscle activity      | +       | +       |
| Voice intonation            | +       | +       |
| Questionnaire               | +       | +       |

The rest of the paper is organized as follows: Section 2 explains the proposed method. Experimental result and their analysis are presented in Section 3 and finally, in Section 4, the paper is concluded and future works discussed.

2. Proposed Method

Many learning models and training loss functions have already been proposed for emotion recognition. This work introduces an additional new loss function and performs experiments using multiple existing model architectures and sequence lengths in training to prove its effectiveness. The ResNet50 model is selected as the proposed loss function evaluation model. One of the main emotion recognition problems in sequence data is defining interrupted and continuous data. Based on our previous paper [17], in the current work, a new specific loss function is introduced to deal with the issue. Fig.1 shows the flow of the proposed method.

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| Facial muscle activity      | +       | +       |
| Voice intonation            | +       | +       |
| Questionnaire               | +       | +       |
2.1.1 Mean squared error
The first most comparative metric criterion is the Mean Squared Error (MSE), defined as:

\[ \text{MSE} = \frac{1}{N} \sum_{i=1}^{N} (x_i - y_i)^2 \]  

(1)

where \( x_i \) predictions including (valence-arousal) values and \( y_i \) annotations (valence-arousal), and \( N \) is the total number of samples. The MSE calculates an approximate indication of how the obtained training model is performing. A small value of MSE is desirable.

2.1.2 Concordance correlation coefficient
The second one is the Concordance Correlation Coefficient (CCC) [23]. It is widely used to measure the performance of dimensional emotion recognition methods, e.g., in the Aff-Wild challenge [26]. CCC calculates the similarity between two time-series (e.g., all video annotations and predictions) by scaling their correlation coefficients with their mean square difference. The predictions that are well correlated with the annotations but shifted in value are penalized in proportion to the deviation. CCC values are in the range \([-1, 1]\), where +1 indicates perfect concordance and -1 denotes discordance. The higher the value of the CCC, the better the fit between annotations and predictions. The mean value of CCC for valence and arousal estimation was used as the main evaluation criterion.

CCC is defined as follows:

\[ \rho_c = \frac{2s_{xy}}{s_x^2 + s_y^2 + (\bar{x} - \bar{y})^2} = \frac{2s_x s_y \rho_{xy}}{s_x^2 + s_y^2 + (\bar{x} - \bar{y})^2} \]  

(2)

where \( \rho_{xy} \) is the Pearson Correlation Coefficient (Pearson CC), \( s_x \) and \( s_y \) are the variances of all valence or arousal video annotations and predicted values, respectively and \( s_{xy} \) is the corresponding covariance value, \( \bar{x} \) and \( \bar{y} \) mean values of predictions and annotations.

2.1.3 Proposed non-inertial loss function
Two criteria are measured for evaluating the performance of networks. Valence and Arousal’s fractional range is between \([-1, 1]\). The problem is that there is no loss function to quickly train the networks on less data. Moreover, Valence and Arousal are not separated values, and it is usually considered important to train them together in a coordinate system of points. This work uses the unit circle map of V-A. This new definition is named the "Non-Inertial loss".

The new loss function for the V-A is defined by the following equations.

\[ \Delta l_c = \sqrt{x_c^2 - y_c^2} \]  

(3)

\[ \Delta l_{x,y} = (\sqrt{(x_c(v) - x_p(v))^2 + (y_c(a) - y_p(a))^2} - \sqrt{(y_c(v) - y_p(v))^2 + (y_c(a) - y_p(a))^2}) / t \]  

(4)

\[ \Delta \alpha = \tan^{-1} \frac{a_x}{v_x} - \tan^{-1} \frac{a_y}{v_y} \]  

(5)

\[ \text{loss} = \text{mean}((\Delta l_c + \Delta l_{x,y} + \Delta \alpha) \]  

(6)

Equation (3) is referred to as norm 2, Euclidean distance or RMSE of the annotations and predictions, which calculates how far away in V-A unit map the prediction is. A small value for the distances is desired. Equation (4), where \( t \) is time, \( x_c(v) \) is the current prediction valence, and \( x_p(a) \) is the previous prediction arousal, calculates the difference of prediction and annotation V-A velocities. To avoid the network parameters exploding, \( t = 1 \) is assumed. Velocity will be enhanced in the recurrent section of the training model, which in our network is the LSTM layer. Equation (5) is the direction. It calculates the differences of angles. The difference between annotation and prediction angles are expected to become zero; \( a_x \) is the projection of prediction arousal and \( v_y \) is the projection of annotation valence. Differences of angles are converted to avoid subtraction because of zero denominators and value more than 1 is overlooked in the arcsin function. The proof of the Equations (5) is in Appendix A.

\[ \Delta l_{x,y} = (\sqrt{(x_c(v) - x_p(v))^2 + (y_c(a) - y_p(a))^2} - \sqrt{(y_c(v) - y_p(v))^2 + (y_c(a) - y_p(a))^2}) / t \]  

\[ \Delta \alpha = \tan^{-1} \frac{a_x}{v_x} - \tan^{-1} \frac{a_y}{v_y} \]  

\[ \text{loss} = \text{mean}((\Delta l_c + \Delta l_{x,y} + \Delta \alpha) \]  

\[ Fig. 2 Non-inertial loss function illustration \]  

The non-inertial loss function works with the form \([\text{batch, sequence, } 2]\), which is our annotation size. If
the annotation size is more than 2, then an acceleration parameter can be added and the circle of angle difference can be extended from the first column to the end.

Fig. 2 shows an illustration of an example loss function annotation and prediction sequence in arousal and valence map.

2.2 Proposed training model

The proposed model (Full Net) is illustrated in Fig. 3. It consists of three stages. The first stage inputs the openPose features. The second stage consists of the Linear layers, and the last stage is a Recurrent stage LSTM, which is widely used and already proven effective in Action Recognition [16]. The first stage extracts a feature representation of a snippet, which consists of a facial RGB image, face landmarks, body pose, and Mel spectrogram features. The RGB image is fed into the ResNet50 network. The sequence of extracted features of openPose outputs is fed directly into the second stage linear layers. The output of the linear layers feeds the last stage of the LSTM network and classifier. For low-cost training, features were extracted using a pre-trained ResNet50 in our previous study [17]. In this work, only openPose and pre-trained ResNet50 are not trainable. All other parameters are trained. Moreover, to test the proposed loss functions in different network parameter sizes, the Full network is split into 3 additional models; "Without mel Network", "Audio Network", and "Pose Network". For interrupted data network, "Without mel Network" and "Pose Network", are used because of input data interruption, that is, when there is no detected pose estimation and face features from openPose. For "Full Network" and "Audio Network", representation of continuous networks is assumed. All these candidate networks are trained using the 3 loss functions.

2.3 Training data

Mollahosseini et. al. [20] deal with the largest database for Emotion Recognition in a Wild setting referred to as Aff-Wild [26]. The database contains more than 30 hours of footage in 298 videos. To satisfy the "in the wild" concept, data videos specifically not made for any specific task of emotions recognition are required. Hence, the videos were gathered from YouTube using the keyword "Reaction". Most contained people who naturally reacted to unexpected plots, exciting situations, etc. The data also contains the Training and Test videos, facial bounding box, facial landmark, and target, in two dimensions, Arousal and Valence. From the training data, the following two features are extracted for training, Mel spectrogram, and openPose. They are briefly described below.

2.3.1 Mel spectrogram

Frequency Mel-scale describes the perceptual distance between pitches of different frequencies. A classical approximation is to define the frequency-to-mel transform function for a frequency $f$ as

$$m = 2595 \cdot \log_{10}(1 + \frac{f}{700})$$

Our method uses Mel-frequency Spectrogram as input to the Linear layers. Spectrograms are generated when Short Term Fourier Transform (STFT) is applied on windowed audio or speech signal. The audio is sampled at 22050Hz. Windowing is then carried out on each audio frame using a "Hann" window of length 2048. Fast Fourier Transform (FFT) windows of length 2048 are then applied on the said windowed audio samples with an STFT hop-length equal to 512. The obtained Spectrogram magnitudes are then mapped to the Mel-scale to get Mel-spectrograms. 128 Spectrogram coefficients per window are used in this model. The Mel-frequency scale emphasizes the lower end of the frequency spectrum over the higher ones, thus, imitating the perceptual hearing capabilities of humans. The "librosa" python package, along with the above-mentioned parameters are used to compute the Mel-spectrograms. In speech emotion recognition, Chan et al. [19] previously researched this topic. A sample Spectrogram corresponding to Aff-Wild training 110.avi audio is shown below in Fig.4.

2.3.2 OpenPose

Human 2D pose estimation is a method for localizing human body parts such as the shoulders, elbows, and ankles from an input image or video. openPose [24], developed by researchers at the Carnegie Mellon University can be considered as the state of the art approach for real-time human pose estimation. A sample Body and Face key points corresponding to Aff-Wild training video number 110.avi and frame 5389 is shown below in Fig.5 and 6. The two green crosses in Fig.5 and 6 are the nose key points, at same location. A previous study also used body pose in video emotion recognition [15].

3. Experiments and Results

The four training networks used for evaluation of the proposed Non-inertial loss function are implemented as follows:

3.1 Training network details

1. Full Network: The network architecture is shown in Fig.3. The flow is as follows.
The Input (Batch(B), Sequence(S), Height(H), Width(W), Channel(C)) feed the openPose to get pose estimation and face features. Face feature coordination is used to calculate and pre-process the face with a bounding box and then feed into ResNet50 network. The previous layer output is concatenated with the face landmarks \((B \times S, 2048 + 140)\) and fed into the linear layer named Landmark. The landmark layer directly feeds into the Pose layer \((B \times S, 1024 + 36)\). After the Pose layer, Mel layer continuous input is \((B \times S, 512 + 128)\). Mel layer output is \((B \times S, 256)\) which is directed as input into the LSTM layer \((B, S, 256)\). The LSTM layer requires additional Sequence dimension, the dimension of Batch, Sequence, and output of previous layers. At the end of the classifier layer \((B, S, 2)\) the final outputs are calculated.

2. Without mel Network: This network does not include continuous input Mel spectrogram and Mel layer. Other parameters are the same as the previous Full Network.

3. Audio Network: Input \((B \times S, 128)\) continuous audio data is fed into Mel layer and output is \((B \times S, 256)\). Before the LSTM layer, a new dimension of sequence \((B, S, 256)\) is added. The end Classifier linear layer \((B, S, 2)\) classifies arousal and valence.

4. Pose Network: As non-continuous data, Pose data Input \((B \times S, 36)\) is fed into the Pose layer. Also, the dimension of sequence \((B, S, 256)\) is added and fed into LSTM \((B, S, 256)\) layer. This is the same as the previous networks. The classifier layer \((B, S, 2)\) also classifies arousal and valence.

All the network configurations used batch normalization 1D and dropout 0.5 after every fully connected layer.

3.2 Data pre-processing

Initially, for all the train and test sets, all body pose and facial landmarks are extracted using openPose [24]. From this output, objective personal data is obtained, using landmarks, by calculating a new facial bounding box expanded 5 pixels and then resizing it to 224x224 pixels. This facial bounding box was applied to extract features on the sequential image using the
The ResNet50 network obtained the final linear layer output and saved 2048x1 features with facial landmarks (70x2) and body pose (18x2). Moreover, from the video, the audio signal was separated and converted to the Mel-Spectrogram features. All training and validation data are normalized to between 0 and 1.

3.3 Experimental configuration

Training: All the following configurations were similar in the 4 candidate networks. The Aff-Wild dataset was split into 2 Train and Validation sets as 70%:30% and 90%:10% respectively to make sure that our loss function and models are accurate for both standard or less training and validation data proportions. During training, the 3 loss functions and the standard stochastic gradient descent optimizer, with momentum (0.9) and weight decay \((5e^{-4})\) were used. The number of epochs was set to 70. Early stopping (15 epochs) was used to prevent over-fitting. The Learning rate was 0.01 with the scheduler (patience 10 epochs). Batch size was set at 64, with the Sequence length varied in Validation:30% [32, 64, 128, 256, 384] and Validation:10% [128, 256, 512]. However, because different experiments had different GPU consumption, the largest batch size that fits in Train and Validation set video length and our GPU memory (11GB) was chosen. However, some of Validation:30% video sequences were less than 512, the max sequence length was reduced to 384. Iteration of data-loader, drop last, and shuffle parameters were set to False. Train and validation video sets were shuffled at the beginning of each epoch. The pre-trained ResNet50 model weights were fixed during training; all the other layers were trainable. Batch normalization and dropout were used after every fully connected layer.

Validation: The losses of MSE, Non-Inertial, and CCC were calculated in each video and sample output of arousal and valence saved using TensorFlow SummaryWriter. Additionally, all the best losses of the model were saved for the rest of the test set.

3.4 Results

Due to comparison difficulty, the base unit in the CCC loss score was set as the base, which in training, \(VA = -2\) is the best loss, and in validation, 2 is the best score. The 3 loss functions trained on the Aff-Wild dataset was observed in 2 ways: 5 times trained for stability check-in 4 networks and split/trained candidates of the 4 networks in training and validation data set proportions 70% : 30% and 90% : 10% among the configuration sequence length.

3.4.1 Validation 30%, 10%

In the train and validation, pipeline batch iteration took around 0.01sec, which as expected, was fast enough even though it was the same when max sequence length 512 was used. Fig.7 shows the comparison of our loss function, MSE, and CCC in various network parameter size space. From this result, the new loss function was sensitive for network parameter size like the MSE function. In our candidate four networks, "Pose Net" input size is \([B, S, 36]\) normalized pose coordinates, which is small enough. The relation between pose and emotion is 0.163, which shows a very weak correlation.

![Fig. 7 Parameter size vs loss (average sequence length val 10%)](image)

Another expectation of the result in the "Audio Net" mean was 0.206, which shows intonation and emotion as weakly correlated. "Without Mel" and "Full Net" did not produce any notable difference in the CCC correlation. The results of these two networks’ were 0.339 and 0.324, respectively. On the other hand, in these networks’ training, our loss function shows the best result.

![Fig. 8 Sequence length vs loss (full networks val 10%)](image)

In Fig.8, the four networks were trained using various sequence length 128, 256, 512 and validation 10% proportion with the 3 loss functions. The result is
the average of four candidate networks. From the result, the CCC loss shows the top result, because the CCC calculation uses \([\text{std, mean}]\) values of prediction, which is more advanced. On the other hand, these values showed some disadvantage if sequence length were not comfortable, as shown in Fig. 8 and 9.

Fig. 9 Sequence length vs loss (full networks Val 30%)

Fig. 10 Parameter size vs loss (average sequence length Val 30%)

Next, the Validation:30% proportion was experimented on to verify that the result is the same as the previous experiment with additional sequence lengths. In Fig.10, for the training mean sequence length in "Full Net" and "Without mel", our loss function shows the best result and is 0.07 lower than 10% proportion. In Fig.9 the lower sequence length was extended to prove that the CCC loss has a disadvantage if sequence length in a small range is chosen. The loss would be worse than the other losses, which shows that in GPU memory a trade-off between sequence length with parameter size and accuracy may be necessary. Fig.11 shows the average of the previous two training sessions in different proportions of the Validation set. In the results of "Without Mel" and "Full Net" there is no big difference. In addition, the other two loss functions especially our new loss was shown to be stable and produced the best results among different sequence lengths.

3.4.2 5-fold training

The Full network was trained five times, with a sequence length of 256, which was shown as optimal in previous training and the result of this training are shown in Table 2, where rows represent validation's main loss function and column shows parallel calculated losses. In Fig.12, the 5 training Average Line of Non-Inertial and MSE losses were nearly constant. It should be noted that the CCC loss average rapidly increased, which shows it is less stable than our new loss function. The other 3 networks training results are also shown in Table 4 Appendix B.

Fig. 11 Parameter size vs loss (total)

Fig. 12 Full net 5 training CCC loss comparison (sequence 256 val 10%)

3.4.3 Example valence and arousal of full network

Figures 13, 14, and 15 show our new loss function training and sample outputs for arousal and valence. Figures 16, 17 and 18 are the CCC loss training and sample output of the Validation video 158.avi. The best loss on "Full Net" in Validation was 0.86 for Arousal and 0.404 for Valence, for which back-propagation was done separately. Also, in Fig.17 Arousal was positively correlated but missed the constant value. In Figures 13, and 16 training epochs was
| Train Loss | Train | MSE  | CCC  | Non-Inertial Average | Differences | Sum     |
|------------|-------|------|------|----------------------|-------------|---------|
| MSE        | 1     | 0.209 | 0.331 | 0.105                | 0.210       | 0.0000014 |
|            | 2     | 0.211 | 0.346 | 0.107                | 0.210       | 0.0000005 |
|            | 3     | 0.207 | 0.366 | 0.104                | 0.210       | 0.0000116 |
|            | 4     | 0.225 | 0.337 | 0.113                | 0.210       | 0.0002326 |
|            | 5     | 0.199 | 0.333 | 0.100                | 0.210       | 0.0001291 |
| CCC        | 1     | 0.348 | 0.300 | 0.176                | 0.316       | 0.0000454 |
|            | 2     | 0.364 | 0.282 | 0.191                | 0.316       | 0.0011459 |
|            | 3     | 0.335 | 0.321 | 0.170                | 0.316       | 0.0000262 |
|            | 4     | 0.415 | 0.319 | 0.213                | 0.316       | 0.000107  |
|            | 5     | 0.271 | 0.348 | 0.136                | 0.316       | 0.0010367 |
| Non-Inertial| 1    | 0.202 | 0.411 | 0.102                | 0.103       | 0.0000025 |
|            | 2    | 0.206 | 0.355 | 0.104                | 0.103       | 0.0000006 |
|            | 3    | 0.204 | 0.414 | 0.103                | 0.103       | 0.0000000 |
|            | 4    | 0.202 | 0.415 | 0.102                | 0.103       | 0.0000016 |
|            | 5    | 0.209 | 0.376 | 0.105                | 0.103       | 0.0000047 |

70 but the training sessions did not reach 40 epochs in some models because of early stopping.

Fig. 13 Full network validation CCC loss (Non-inertial training)

Fig. 14 Non-inertial loss example validation of arousal (158.avi)

Fig. 15 Non-inertial loss example validation of valence (158.avi)

Fig. 16 Full network validation CCC loss (CCC training)

4. Discussion

This work shows that the proposed new loss function has an advantage if we choose the correct network...
pipeline. Fig. 11 shows the average of the previous two training sessions in different proportions of the validation set. In the results of “Without Mel” and “Full Net” there is no big difference. This is because the Aff-Wild set audio was used directly without any preprocessing and transcribing.

From Table 1, the emotion parameters relation used is “Facial expression”, “Facial muscle activity” and “Voice intonation”. In addition, new relations for “Body pose” and emotion were added. Consequently, the representations of interrupted networks “Without mel Network” and “Pose Network” accuracy was lower than the continuous networks, which shows the data interruption effect. Moreover, our loss function training on “Full net” was acceptable, excluding fitting annotation explosion in the vertical axis. It could be easily fixed by another network design, that is more deep or wide.

Our promised contributions in Section 1., are as follows:

1. In the proposed loss function, the angle difference calculation allowed for more accurate Arousal and Valence through back-propagation compared to the other loss functions. The results are shown in Figures 14, 15, 17, and 18

2. Figures 8 to 9 shows our proposed loss function trained more accurately on less data.

3. Additionally, as shown in Table 2, our loss function provides better accuracy training on ”5 training” data.

4. In training and validation, pipeline batch iteration took around 0.01 sec, that as expected, was fast enough even though it was the same for the max sequence length 512.

5. Conclusion

In this work, we proposed a new loss function named ”Non-Inertial Loss” and proved its stability and effectiveness using four networks designed with different sequence lengths, and validation proportion. We observed that, in data relation for continuous and interrupted data, if the network and data were low, the interruption effect was high. Conversely, if data and networks were large, the interruption effect was low.

Our loss function was limited by a smaller network parameter size, just like the other existing losses (CCC and MSE). However, in the sequence range, our loss function showed better results in the lower rank, which allows better trade-off cost between the network size and sequence length.

In the future, we will continue to test the new loss function with acceleration detailed in Appendix A. We will also evaluate this new loss function using other states of the art networks to see how it improves emotion recognition accuracy.

Appendix

Extended proposed loss function

\[
Distance = \frac{1}{N} \sum_{i=1}^{N} (x_i - y_i)^2 \quad (8)
\]

\[
Velocity = \left| \frac{1}{NM} \sum_{i=1}^{N} \sum_{j=1}^{M} \frac{\partial x_{i,j}}{\partial t} - \frac{\partial y_{i,j}}{\partial t} \right| \quad (9)
\]

\[
Alpha = \tan^{-1} \frac{a_x}{v_x} - \tan^{-1} \frac{a_y}{v_y} = \left| \frac{1}{N(M+1)} \sum_{i=1}^{N} \sum_{j=1}^{M} \left( \frac{\partial x_{i,j}}{\partial t} \frac{\partial y_{i,j+1}}{\partial t} - \frac{\partial y_{i,j}}{\partial t} \frac{\partial x_{i,j+1}}{\partial t} \right) \right| \quad (10)
\]

\[
Acceleration = \left| \frac{1}{NM} \sum_{i=1}^{N} \sum_{j=1}^{M} \frac{\partial^2 x_{i,j}}{\partial t^2} - \frac{\partial^2 y_{i,j}}{\partial t^2} \right| \quad (11)
\]
\[ \text{loss} = \frac{D + V + A + Ac}{4} \]  

(12)

Proof of Equation 5:

\[ \Delta \alpha = \tan^{-1} \frac{a_x}{v_x} - \tan^{-1} \frac{a_y}{v_y} \Rightarrow \]

\[ \lim_{\Delta \alpha \to 0} \Delta \alpha = 0 \Rightarrow \]

\[ 0 = \tan^{-1} \frac{a_x}{v_x} - \tan^{-1} \frac{a_y}{v_y} = \]

\[ \tan(0) = \frac{a_x}{v_x} = \frac{a_y}{v_y} \Rightarrow \]

\[ 0 = \frac{a_x}{v_x} * v_y - \frac{a_y}{v_y} * v_x \Rightarrow \]

\[ \Delta \alpha = a_x * v_y - a_y * v_x \]

(13)

Proof of Equation 5 in an example:

assume

\[ \angle \text{annotation} = 90^\circ \]

\[ \angle \text{prediction} = 30^\circ \]

\[ \Delta \alpha = 90^\circ - 30^\circ = 60^\circ \Rightarrow \]

\[ a_x = \sin(\pi/2) = 1 \quad v_x = \cos(\pi/2) = 0 \]

\[ a_y = \sin(\pi/6) = 1/2 \quad v_y = \cos(\pi/6) = \sqrt{3}/2 \]

\[ \sin(A - B) = \sin(A) * \cos(B) - \cos(A) * \sin(B) \]

\[ \Delta \alpha = \arcsin(a_x * v_y - a_y * v_x) \]

\[ \Delta \alpha = \arcsin(1 * \sqrt{3}/2 - 0 * 1/2) \]

\[ \Delta \alpha = \arcsin(\sqrt{3}/2) = 60^\circ \]

\[ 60^\circ = 60^\circ \]  

(14)

Training tables

Table 3 Validation: 10% training

| Network     | Train Loss | Sequence Length | MSE | CCC   | Non-Inertial |
|-------------|------------|-----------------|-----|-------|--------------|
| Full Network|            |                 |     |       |              |
| MSE         | 128        | 0.233           | 0.374 | 0.117 |
|             | 256        | 0.245           | 0.312 | 0.123 |
|             | 512        | 0.229           | 0.288 | 0.115 |
| CCC         | 128        | 0.303           | 0.338 | 0.161 |
|             | 256        | 0.380           | 0.262 | 0.195 |
|             | 512        | 0.216           | 0.404 | 0.109 |
| Non-Inertial |            |                 |     |       |              |
| MSE         | 256        | 0.214           | 0.344 | 0.109 |
|             | 512        | 0.217           | 0.319 | 0.109 |
| Without mel |            |                 |     |       |              |
| MSE         | 256        | 0.216           | 0.277 | 0.112 |
|             | 512        | 0.223           | 0.254 | 0.112 |
| Audio Network|          |                 |     |       |              |
| MSE         | 256        | 0.210           | 0.375 | 0.110 |
|             | 512        | 0.214           | 0.335 | 0.109 |
| Non-Inertial |            |                 |     |       |              |
| MSE         | 256        | 0.199           | 0.202 | 0.100 |
|             | 512        | 0.190           | 0.262 | 0.100 |
| Pose Network |           |                 |     |       |              |
| MSE         | 128        | 0.231           | 0.300 | 0.116 |
|             | 256        | 0.252           | 0.349 | 0.126 |
|             | 512        | 0.256           | 0.274 | 0.129 |
| Non-Inertial |            |                 |     |       |              |
| MSE         | 128        | 0.213           | 0.151 | 0.107 |
|             | 256        | 0.208           | 0.141 | 0.105 |
|             | 512        | 0.214           | 0.165 | 0.107 |
| Pose Network |           |                 |     |       |              |
| MSE         | 128        | 0.234           | 0.103 | 0.118 |
|             | 256        | 0.232           | 0.150 | 0.117 |
|             | 512        | 0.222           | 0.134 | 0.112 |
| CCC         | 128        | 0.305           | 0.230 | 0.180 |
|             | 256        | 0.239           | 0.255 | 0.179 |
|             | 512        | 0.475           | 0.176 | 0.247 |
| Non-Inertial |            |                 |     |       |              |
| MSE         | 128        | 0.222           | 0.126 | 0.112 |
|             | 256        | 0.229           | 0.151 | 0.115 |
|             | 512        | 0.225           | 0.144 | 0.113 |
### Table 4: Training (sequence 256 val 10%)

| Network          | Train Loss | Fold | MSE     | CCC | Non-Inertial |
|------------------|------------|------|---------|-----|--------------|
| **Full Network** | MSE        | 1    | 0.209   | 0.331| 0.105        |
|                  |            | 2    | 0.211   | 0.346| 0.107        |
|                  |            | 3    | 0.207   | 0.366| 0.104        |
|                  |            | 4    | 0.225   | 0.337| 0.113        |
|                  |            | 5    | 0.199   | 0.333| 0.100        |
|                  |            | 6    | 0.348   | 0.309| 0.176        |
|                  |            | 7    | 0.361   | 0.282| 0.191        |
|                  |            | 8    | 0.355   | 0.321| 0.170        |
|                  |            | 9    | 0.415   | 0.319| 0.213        |
|                  |            | 10   | 0.271   | 0.348| 0.136        |
|                  |            | 11   | 0.202   | 0.411| 0.102        |
|                  |            | 12   | 0.206   | 0.355| 0.104        |
|                  |            | 13   | 0.204   | 0.414| 0.103        |
|                  |            | 14   | 0.202   | 0.415| 0.102        |
|                  |            | 15   | 0.209   | 0.376| 0.105        |

### Table 5: Validation: 30% training

| Network          | Train Loss | Sequence Length | MSE     | CCC | Non-Inertial |
|------------------|------------|-----------------|---------|-----|--------------|
| **Full Network** | MSE        | 32              | 0.203   | 0.258| 0.102        |
|                  |            | 64              | 0.201   | 0.251| 0.101        |
|                  |            | 128             | 0.204   | 0.265| 0.103        |
|                  |            | 256             | 0.196   | 0.254| 0.100        |
|                  |            | 384             | 0.206   | 0.230| 0.104        |
|                  |            | 64              | 0.371   | 0.177| 0.192        |
|                  |            | 128             | 0.291   | 0.289| 0.148        |
|                  |            | 256             | 0.274   | 0.287| 0.144        |
|                  |            | 384             | 0.281   | 0.283| 0.149        |
|                  |            | 64              | 0.207   | 0.284| 0.101        |
|                  |            | 128             | 0.193   | 0.322| 0.097        |
|                  |            | 256             | 0.194   | 0.260| 0.098        |
|                  |            | 384             | 0.203   | 0.271| 0.102        |
| **Without mel Spectrogram** | MSE        | 32              | 0.203   | 0.259| 0.102        |
|                  |            | 64              | 0.217   | 0.253| 0.110        |
|                  |            | 128             | 0.202   | 0.241| 0.102        |
|                  |            | 256             | 0.202   | 0.222| 0.102        |
|                  |            | 384             | 0.208   | 0.201| 0.105        |
|                  |            | 64              | 0.359   | 0.229| 0.180        |
|                  |            | 128             | 0.325   | 0.262| 0.168        |
|                  |            | 256             | 0.268   | 0.290| 0.140        |
|                  |            | 384             | 0.287   | 0.275| 0.132        |
|                  |            | 64              | 0.208   | 0.243| 0.105        |
|                  |            | 128             | 0.191   | 0.285| 0.096        |
|                  |            | 256             | 0.194   | 0.234| 0.097        |
|                  |            | 384             | 0.195   | 0.290| 0.098        |
| **Audio Network** | MSE        | 32              | 0.213   | 0.202| 0.107        |
|                  |            | 64              | 0.205   | 0.205| 0.103        |
|                  |            | 128             | 0.201   | 0.184| 0.101        |
|                  |            | 256             | 0.184   | 0.192| 0.098        |
|                  |            | 384             | 0.200   | 0.180| 0.101        |
|                  |            | 64              | 0.214   | 0.252| 0.125        |
|                  |            | 128             | 0.231   | 0.278| 0.116        |
|                  |            | 256             | 0.254   | 0.300| 0.126        |
|                  |            | 384             | 0.254   | 0.289| 0.118        |
|                  |            | 64              | 0.202   | 0.184| 0.102        |
|                  |            | 128             | 0.199   | 0.162| 0.100        |
|                  |            | 256             | 0.191   | 0.177| 0.096        |
|                  |            | 384             | 0.195   | 0.171| 0.098        |
| **Pose Network**  | MSE        | 32              | 0.229   | 0.059| 0.115        |
|                  |            | 64              | 0.213   | 0.082| 0.109        |
|                  |            | 128             | 0.209   | 0.094| 0.105        |
|                  |            | 256             | 0.204   | 0.129| 0.103        |
|                  |            | 384             | 0.207   | 0.134| 0.104        |
|                  |            | 64              | 0.373   | 0.045| 0.194        |
|                  |            | 128             | 0.365   | 0.157| 0.193        |
|                  |            | 256             | 0.350   | 0.213| 0.119        |
|                  |            | 384             | 0.265   | 0.091| 0.133        |
|                  |            | 64              | 0.212   | 0.104| 0.106        |
|                  |            | 128             | 0.207   | 0.056| 0.104        |
|                  |            | 256             | 0.204   | 0.118| 0.103        |
|                  |            | 384             | 0.202   | 0.154| 0.101        |
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Jargalsaikhan Orgil is a Lecturer at the School of Information and Communication Technology of Mongolian University of Science and Technology. Since 2018, he has been a doctoral course student at the Graduate School of Technology. His research interests include emotion recognition, image processing and deep learning.
Stephen Karungaru received his B.S degree from the Department of Electrical and Electronics, Moi University, Kenya. He received his master's and doctoral degrees from the Department of Information Science and Intelligent Systems, Faculty of Engineering, Tokushima University, in 2001 and 2004, respectively. He became an Associate Professor, Graduate School of Technology, Industrial and Science, Tokushima University in 2004. His research interests are in face detection, recognition, neural networks, and genetic algorithms.

Kenji Terada received his B.E., M.E., and Dr.Eng. degrees in electrical engineering, all from Keio University, Japan in 1990, 1992 and 1995, respectively. He is currently a Professor at Tokushima University. His research interests include the image processing, and computer vision.

Ganbold Shagdar is an Associate Professor in the School of Information and Communication Technology of Mongolian University of Science and Technology (MUST). He is a member of IEEE. He received his B.S. and M.S degrees in electronic engineering from MUST, Ulaanbaatar, Mongolia, in 1991 and 1997, respectively, and Ph.D. degree from Gwangju Institute of Science and Technology, Gwangju, Korea, in 2016. His current research interests include dynamic wavelength and bandwidth allocation, energy efficiency and resilient architecture in optical access networks, optical cross connection architectures, and optical transport network.

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