TGMI: an efficient algorithm for identifying pathway regulators through evaluation of triple-gene mutual interaction

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ABSTRACT

Despite their important roles, the regulators for most metabolic pathways and biological processes remain elusive. Presently, the methods for identifying metabolic pathway and biological process regulators are intensively sought after. We developed a novel algorithm called triple-gene mutual interaction (TGMI) for identifying these regulators using high-throughput gene expression data. It first calculated the regulatory interactions among triple gene blocks (two pathway genes and one transcription factor (TF)), using conditional mutual information, and then identifies significantly interacted triple genes using a newly identified novel mutual interaction measure (MIM), which was substantiated to reflect strengths of regulatory interactions within each triple gene block. The TGMI calculated the MIM for each triple gene block and then examined its statistical significance using bootstrap. Finally, the frequencies of all TFs present in all significantly interacted triple gene blocks were calculated and ranked. We showed that the TFs with higher frequencies were usually genuine pathway regulators upon evaluating multiple pathways in plants, animals and yeast. Comparison of TGMI with several other algorithms demonstrated its higher accuracy. Therefore, TGMI will be a valuable tool that can help biologists to identify regulators of metabolic pathways and biological processes from the exploded high-throughput gene expression data in public repositories.

INTRODUCTION

It is known that most organisms have at least several hundred metabolic pathways and a multitude of biological processes, but our understanding of how these biological pathways or processes are regulated is limited. For example, Arabidopsis thaliana has 549 annotated metabolic pathways and a few thousand biological processes as defined with gene ontology terms, but the regulators for most of these pathways have not yet been revealed (1–3). With the advent of the whole-genome approach and the explosion of biological data in public repositories, demands have heightened for computational algorithms that can be used to predict pathway regulators using high-throughput gene expression datasets. Although some methods for building gene regulatory networks have been developed during the last decade, accurate algorithms tailored specifically for identifying pathway regulators have not been developed. Currently, methods for identifying regulatory relationships from time-series gene expression data include dynamic Bayesian networks (4–6), differential equations (7), control logic (8), Boolean networks (9), stochastic networks (10) and finite state linear models (11). These methods and algorithms are primarily suitable for time-course data generated from bacteria, yeast and some cell lines of eukaryotic organisms.

Gene expression datasets in public repositories have increased exponentially. Most are non-time series static gene expression datasets, which include both treatment versus control datasets and those that have very large time intervals of a few hours to even several days (12). During each time interval, too many biological events elapsed to abolish the attempt to perform dynamic simulation using temporal variables. A few highly efficient methods have...
been developed to infer regulatory relationships from these types of static data, such as the Algorithm for the Reconstruction of Accurate Cellular Networks (ARACNE) (13), the Backward Elimination Random Forest (BWERF) algorithm (14), and the Bottom-up Graphical Gaussian Model (Bottom-up GGM) algorithm (15,16). The ARACNE algorithm uses 'mutual information' to identify dependent relationships between pairwise genes and then applies a data processing inequality to remove indirect links. It can therefore be used to identify pathway regulators through analysis of transcription factor (TF)-pathway gene dependence. BWERF and Bottom-up GGM were developed and tailored for building multilayered hierarchical gene regulatory networks (ML-hGRNs) that operate above a given pathway. BWERF is based on a random forest algorithm with a recursive evaluation process to reduce the number of TFs that have greater importance values to pathway genes; this process is repeated with the newly acquired layer to be set as the new bottom layer and the rest of TFs until a multi-layered ML-hGRN is obtained. The Bottom-up GGM method also constructs a ML-hGRN using a set of pathway genes as the bottom layer and TFs as inputs for building multiple upper layers in a layer-by-layer fashion. When Bottom-up GGM method is used to evaluate the significant interference within a triple gene block, i.e. the interference of a candidate TF in the higher hierarchical layer on two pathway genes. The interference can be determined by examining whether the difference between the correlation coefficient of two pathway genes and the partial correlation coefficient of the two bottom-layer genes after removing the effect of the upper-layer TF exceeds the significance level. This difference represents the interference strength of the TF on the two bottom-layer genes.

In this study, we present a novel algorithm called triple-gene mutual interaction (TGMI) for identifying regulators of metabolic pathway and biological process from high-throughput gene expression data by evaluating triple gene blocks. The reasons that we used triple gene blocks instead of other combinations of genes in TGMI are based on two biological and one statistical facts. First, genes involved in the same pathway or biological process are tended to be coexpressed (17) or coordinated (18,19) in expression patterns. Second, genes with same or similar expression patterns are often under the regulation of the same molecular mechanism (20–22). Third, several studies also showed that the evaluation of three variables together is more powerful than the evaluation of two variables for recognizing causal relationships (43,86,87). TGMI algorithm therefore used each paired pathway genes as a ‘bait’ to fish the TFs that had highest regulatory interactions with two pathway genes. When applied to a gene expression dataset, it first dissected all interactions among a triple gene block into seven interactive components, based on which we developed an efficient measure to screen for the significantly interacted triple gene blocks in which paired pathway genes have dependency while TFs and paired pathway genes showed significant conditional interactions. Then, the frequencies of all TFs’ presence in significantly interacted triple gene blocks were calculated and ranked to show the importance of each TF to a pathway or a biological process. The algorithm was applied to several metabolic or non-canonical pathways using microarray gene expression data from A. thaliana and mouse embryonic stem cells. The ranked TFs were compared with those obtained from the other three algorithms, BWERF, Bottom-up GGM and ARACNE, using the same input data. The results indicated that the TGMI algorithm was more efficient and accurate in identifying true pathway regulators than the other three algorithms.

**MATERIALS AND METHODS**

**Arabidopsis thaliana microarray gene expression datasets**

A wood formation compendium dataset (128 microarray samples) was constructed using the microarray data from A. thaliana hypocotyledonous stem tissue treated under short-day condition that is known to induce wood formation (23). These data are publicly available in the NCBI GEO repository (http://www.ncbi.nlm.nih.gov/geo/) with the following accession numbers: GSE607, GSE6153, GSE18985, GSE2000, GSE24781 and GSE5633. Affymetrix 25k ATH1 microarrays were used to generate all these datasets. The CEL files were downloaded and processed with the Robust Multi-Array Analysis algorithm available at https://www.bioconductor.org (24). A previously published method was used to perform quality control of the datasets (25).

**Mouse microarray gene expression datasets**

Pluripotency maintenance pathway was downloaded from the embryonic stem cells atlas of pluripotency evidence (ESCAPE) repository. This time-course dataset was generated using the Affymetrix MOE439A arrays from embryonic stem cells under undirected differentiation, with three replications at each of the following time points: at 0, 6, 12, 18, 24, 36 and 48 h, and also 4, 9 and 14 days. Validated regulatory relationships were obtained from ChIP-X studies available in the ESCAPE repository (http://www.maayanlab.net/ESCAPE/). The pluripotency maintenance pathway with 24 genes and 35 known regulatory TFs was used to construct three datasets with 100, 200 or 300 random noise genes for the evaluation of the TGMI algorithm.

**The TGMI algorithm**

The interactions between a regulatory TF and a pair of pathway genes were first evaluated by conditional mutual information plus a novel mutual interaction measure (MIM) we discovered. Given a triple gene block with a TF being represented by a variable $X$ and a pair of pathway genes being represented by variables $Y_1$ and $Y_2$ (Figure 1A), the gene expression data for each gene were discretized by using the equal frequency discretization algorithm (26). The entropy ($H$) of each variable is then calculated using the following formula:

$$H(X) = -\sum_x p(x) \log p(x) = -E[\log(p(x))] ,$$

where $x$ represents each discretized value in $X$ and $p(x)$ is the probability mass function. $H(Y_1)$ and $H(Y_2)$ were calculated in the similar way.

The mutual information between each pair of variables, i.e. $(Y_1, Y_2), (Y_1, X)$ and $(Y_2, X)$, was calculated using the
following formulae. We used \((Y_1, Y_2)\) gene pair as an example to show how to calculate the mutual information, and for the other pairs of variables, \((Y_1, X)\) and \((Y_2, X)\), could be calculated in the similar way.

The conditional entropy, \(H(Y_1|Y_2)\), was calculated as:

\[
H(Y_1|Y_2) = -\sum_{y_1, y_2} p(y_1, y_2) \log p(y_1|y_2)
\]

and the joint entropy, \(H(Y_1, Y_2)\), as:

\[
H(Y_1, Y_2) = -\sum_{y_1, y_2} p(y_1, y_2) \log p(y_1, y_2)
\]

From this, mutual information, \(I(Y_1; Y_2)\), could be obtained:

\[
I(Y_1; Y_2) = H(Y_1) + H(Y_2) - H(Y_1, Y_2)
\]

The S1, S2 and S3 segments as shown in Figure 1B can be represented by the conditional entropies of each variable given the other two variables, i.e. by \(H(Y_1|X, Y_2)\), \(H(Y_2|X, Y_1)\) and \(H(X|Y_1, Y_2)\). S4 is the conditional mutual information of \(Y_1, X\) given \(Y_2\); S5 is the conditional mutual information of \(Y_2, X\) given \(Y_1\); S6 is conditional mutual information of \(Y_1, Y_2\) given \(X\); S7 is the difference between mutual information between \(Y_1, Y_2\) and \(X\). These can be calculated using the definition of multivariate conditional entropy, as follows:

The joint entropy, \(H(Y_1, Y_2, X)\), is calculated in the same way as described in (27).

\[
H(Y_1, Y_2, X) = -\sum_{y_1, y_2, x} p(y_1, y_2, x) \log p(y_1, y_2, x)
\]

From this, the conditional entropy for \(S_1\), \(H(Y_1|X, Y_2)\), can then be calculated as:

\[
H(Y_1|X, Y_2) = H(Y_1, Y_2, X) - H(Y_2, X) - H(X)
\]

S2 and S3 can be calculated in a similar manner. Conditional mutual information for \(S_6\) in Figure 1B, i.e. \((Y_1; Y_2|X)\), can be calculated as:

\[
I(Y_1; Y_2|X) = H(Y_1|X) - H(Y_1, Y_2|X)
\]

Then, multivariate mutual information for \(S_7\), \(I(Y_1; Y_2; X)\) can then be calculated from:

\[
I(Y_1; Y_2; X) = I(Y_1; Y_2) - I(Y_1; Y_2|X)
\]

Note that a positive \(S_7\) indicates there exist significant regulatory interactions in the given triple gene block. If \(S_7\) is negative, there is no regulatory interactions and the given triple gene block should be discarded.

The MIM for a triple gene block is calculated as follows:

\[
MIM = \frac{S_7}{S_1 + S_2 + S_3}
\]

This MIM reflects the regulatory strength exerted by the TF on two pathway genes in the triple gene block. The larger the MIM, the more significant the TF controls two pathway genes.

To test if an MIM calculated from a triple gene block is significant, a P-value for each triple gene block was calculated using the randomized permutation method (28). First, 1000 permuted datasets were created by random permutation of the data vector of the TF in the triple gene block. This randomization of all TF data vectors broke original triple gene blocks and generated many new recombined ones. The MIM for each randomly combined block was then calculated and compared to the MIM of original triple gene block to estimate the permutation P-value. After obtaining P-values for all triple gene combinations, the Benjamini–Hochberg method (Benjamini and Hochberg, 1995) was employed to perform multiple testing correction. Triple gene blocks with a false discovery rate (FDR) less than the significance level of 0.05 were considered to have significant interactions.

The importance of a TF to a pathway in overall is represented by the frequency of this TF’s presence in significant triple gene blocks with an FDR > 0.05. The selec-
ation of top k TFs with highest frequency and then linking them with the pathway genes in significant triple gene blocks led to a two-layered network. Based on this network, we extracted putative combinatorial regulation relationships, namely $T_F - PWG_k - T_F$, representing the kth pathway gene $PWG_k$ is regulated by $T_F$ and $T_F$. Combinatorial regulation refers to multiple TFs control the same target gene directly. Identification of them enables genetic engineering of pathways and biological processes more precisely.

Validation of TGMI algorithm on multiple pathways using high-throughput gene expression data

The TGMI algorithm was tested for its accuracy in identifying pathway regulators and building regulatory layers above several biological pathways using data from A. thaliana hypocotyledonous stem tissues and mouse embryonic stem cells. The pathway genes were downloaded from Arabidopsis Information Resource (https://www.arabidopsis.org/). Alternatively, the genes involved in a biological process defined by gene ontology term can be viewed as non-canonical pathway genes for identification of regulatory layers above pathway genes using TGMI algorithm.

Lignin biosynthesis pathway in A. thaliana. Lignin is the second most abundant plant biopolymer found in secondary cell walls and fibers of wood (29,30). Understanding how lignin is synthesized has long been a research focus of plant biologists and the wood industry because of the importance of lignin in plant structural integrity and stem stiffness (31,32). To identify pathway regulators that govern lignin biosynthesis, we used a compendium dataset that comprised 128 microarray samples (33). The data in this compendium were generated from A. thaliana stem tissues under short-day conditions, which induced secondary wood formation. The expression data of the lignin pathway genes and all the TFs were extracted from this compendium data and were subjected to the analysis by the TGMI algorithm. The performance of TGMI was compared with those of the BWERF, Bottom-up GGM and ARACNE algorithms.

Pigment biosynthesis pathways in A. thaliana. The performance of the TGMI algorithm was also tested with a unified pigment biosynthesis pathway in A. thaliana. In plants, pigments provide a broad range of colors from red and orange to blue and violet, serving as important compounds that attract insects for pollination and protect against ultraviolet-B radiation (34). Previous studies have suggested coordinated activity among four linked plant pigment biosynthesis pathways: the anthocyanin, flavonol, flavonoid, and leucopelar–gonidin and leucocyanidin biosynthesis pathways. Leucopelargonidin and leucocyanidin are colorless intermediates synthesized during the course of colored anthocyanin pigmentation (35). Chemical reactions involving leucopelargonidin and leucocyanidin compounds result in red or pink anthocyanin pigmentation in a variety of plant species including A. thaliana (36). Flavonoids are modified by a number of reactions that contribute to pigment formation in seeds and flowers (37). Visible patterns of anthocyanins in plants are intermediated by chemical compounds synthesized by flavonol biosynthesis (38). In this study, we treated anthocyanin, flavonol, flavonoid, and leucopelar–gonidin and leucocyanidin biosynthesis as a single large unified pigment biosynthesis pathway for identifying pathway regulators. First, we performed a co-expression analysis to identify co-expressed pathway gene pairs across the four pigment pathways; the significantly co-expressed pathway gene pairs were used in triple gene blocks. The co-expression among these four pigmentation-related pathways was analyzed using four different pairwise association methods: Spearman rank correlation coefficients, Pearson product moment correlation coefficients, Kendall rank correlation coefficients (39) and the maximum information coefficient (MIC) (40). Of these methods, the Spearman and Kendall coefficients can capture monotonic relationships, whereas the MIC can capture varying degrees of both linear and non-linear relationships between genes. After removing duplicated pairs, all the significant co-expressed pathway gene pairs identified by these four gene association methods were used in triple gene blocks to identify pigment pathway gene regulators.

Pluripotency maintenance pathway in mouse embryonic stem cells. TGMI was also tested with three mouse microarray datasets we prepared in our previous study from a data with 34 samples, which were originally downloaded from the ESCAPE repository. From this original data, the expression data of 35 TFs that were known to control pluripotency were extracted. Following that, the three datasets, namely, Datasets 1, 2 and 3 all contain 24 genes involved in pluripotency maintenance plus 100, 200 and 300 randomly selected noise genes, respectively. The expression data of these noise genes were simulated. For more detail, please consult our previous publication (14).

Cell cycle pathway in Saccharomyces cerevisiae. The TGMI algorithm was also tested for identifying pathway regulators with a microarray dataset from Saccharomyces cerevisiae (41). 29 cell cycle pathway genes were selected from a previous publication (42), as shown in Supplemental File 1, and all TF in yeast were used. BWERF, Bottom-up GGM and ARACNE algorithms were also used as comparisons.

Comparing the accuracy of TGMI with that of other algorithms

Receiver operating characteristic (ROC) curves were used to compare the accuracy of TGMI algorithm with those of the BWERF, Bottom-up GGM and ARACNE algorithms. A pair of true positive rate (TPR) and false positive rate (FPR) values were calculated for each cut-off point in a TF list sorted in descending order based on interference frequencies on pathway genes. In this study, the cut-off point progressed at one gene each time and the same cut-off points were used to threshold the ranked TF lists obtained from all methods to ensure a fair comparability. The acquired TPR and FPR values for all cut-off points were used to plot the ROC curves. An ROC curve that closely follows the TPR axis and then the upper FPR axis indicates a high accuracy of the algorithm, whereas a curve that is closer to the 45-degree diagonal line indicates a low accuracy. To quantify
RESULTS

Lignin biosynthesis pathway in *A. thaliana*

The triple gene blocks identified by TGMI algorithm with a cut-off significance level of 0.05 were shown in the right panel of Figure 2. The interference frequencies of TFs on pathway genes were displayed in the descending order and the TFs highlighted in red are known positive TFs in existing literature. SND1 is a high hierarchical regulator that controls SND2, SND3, MYB103, MYB85, MYB52, MYB54, MYB69, MYB42, MYB86, MYB61, MYB46, MYB20 and KNAT7 (43–45). TGMI algorithm identified 9 of these 15 TFs (SND1, SND2, SND3, MYB103, MYB85, MYB43, MYB46, MYB86, MYB61). NST1, NST2, VND6 and VND7, the functional NAC family homologs of SND1, regulate the same downstream targets in different cell types (46). TGMI recognized NST1 and NST2. In addition, MYB58 and MYB63, which are transcriptional activators of lignin biosynthesis in the SND1-mediated transcriptional regulatory network (47), were identified by TGMI algorithm. TGMI also identified LBD15 (48), XND1 (49), bZIP6 (50) and GATA12 (51), which are involved in regulating various aspects of secondary cell wall synthesis.

The triple gene blocks with significant regulatory interactions were combined to generate a circular network, as shown in the left panel of Figure 2, with the TFs arranged in a clockwise direction, from the most frequent to the least frequent. Each directed edge from a TF to a pathway gene represents a regulatory relationship. It is perceivable that the known positive lignin pathway regulators, highlighted in a light coral color, are those that were most frequently connected to lignin biosynthesis pathway genes.

Figure 3 showed the ROC curves representing the accuracies of the TGMI, BWERF, Bottom-up GGM and ARACNE algorithms. As what can be observed from the shapes of the ROC curves, the TGMI algorithm showed much higher accuracy than the other three algorithms in identifying lignin pathway regulators. This was supported...
by TGMI’s significantly larger AUROC (0.92), indicating it performed better than the other three algorithms. It should be noted that the performances of BWERF and Bottom-up GGM were based on only one layer of TFs inferred, but these algorithms were originally designed to build ML-hGRNs.

The network resulting from TGMI algorithm can be used to identify the possible combinatorial regulatory genes for each pathway gene. We generated a combinatorial map for the lignin pathway (Figure 4). The frequency of each TF–pathway edge (TFi–PWGk–TFj) present in the triple gene blocks (TFi–PWGk–TFj) is given in parentheses next to each TF. The combinatorial TFs, which have supporting literature evidence for regulating pathway genes, are highlighted in the squares.

Figure 4. Identified combinatorial TFs are depicted in the pathway diagram of lignin biosynthesis. The green oval shapes show pathway genes involved in the lignin biosynthesis. The combinatorial TFs are shown in square shapes. The frequencies of interactions for each TF in significant triple gene blocks (TFi–PWGk–TFj) are given in parentheses next to each TF. The combinatorial TFs, which have supporting literature evidence for regulating pathway genes, are highlighted in the squares.

Pigment biosynthesis pathways in A. thaliana

The co-expression analysis was performed between all pairwise genes involved in the unified pigmentation pathway including anthocyanin, flavonol, flavonoid, and leucopelargonidin and leucocyanidin biosynthesis using Spearman, Pearson, Kendall and MIC coefficients. The identified co-expressed pathway gene pairs were used to bait the regulators. The TFs captured with higher frequency are listed at the right-side in Figure 5 and many of them are functionally associated with the pigment biosynthesis. NFYA5 is a stress-responsive regulator related to anthocyanin synthesis, which controls purple pigmentation under drought conditions (58). NARS1 is involved in anthocyanin pigmentation in the epidermal cells of the A. thaliana (59). ANR1 and ANR2 have been shown to induce the over-accumulation of flavonoid intermediates by suppressing the anthocyanin pathway genes (60). MYB33 and MYB65 are involved in anthocyanin accumulation and seed color pigmentation (61). Overexpression of the SVP3 gene in kiwi fruit has been shown to interfere with anthocyanin biosynthesis in petals (62). ATAF1 is involved in anthocyanin synthesis in A. thaliana in adverse growth conditions (63). HYH is an Arabidopsis bZIP TF that is directly involved in anthocyanin and chlorophyll estimation (64). SPL9 negatively regulates anthocyanin by directly suppressing anthocyanin biosynthesis genes (65). GATA15 is involved in various activities of flavonoid intermediates by suppressing the anthocyanin pathway genes (60). MYB33 and MYB65 are involved in anthocyanin pathway genes involved in anthocyanin pigmentation.

The regulatory network operating above the mouse pluripotent stem cells

The regulatory network operating above the mouse pluripotent stem cells was constructed with TGMI algorithm using mouse Dataset 3, which contains 24 pathway genes, 35 TFs and 300 randomly selected noise genes. The
Figure 5. Regulatory network for the unified pigment biosynthesis pathway that consists of anthocyanin, flavonol, flavonoid, and leucopelargonidin and leucocyanidin biosynthesis. Green nodes represent pathway genes. All other nodes are TFs regardless of their colors. Light coral nodes represent positive known TFs of pigment biosynthesis. References are provided for those positive known TFs that are evidenced to regulate pigment synthesis pathway genes.

Figure 6. The performance of TGMI in recognition of authentic pigment pathway regulators using ROC curves. The ROC curves that closely follow the TPR axis, and then the top FPR axis, represent the higher accuracies in identifying positive regulatory TFs. In the contrary, the ROC curves that more closely follow the 45-degree diagonal line reflect lesser accuracies. AUROC was also calculated and provided for comparing the accuracies of different algorithms.

results were shown in Figure 7A. The TFs recognized by TGMI included 12 positive TFs out of the 35 known TFs involved in pluripotency maintenance in mouse embryonic stem cells: SOX17 (69), NROB1 (70), PHC1 (71), CTCF (72), ZFP42 (73), ZFP281 (74), ESRRB (75), MYCN (76), REST (77), GATA3 (78), MYC (79) and TRIM28 (80). POU5F1, SOX2 and NANOG are well-known master regulatory genes that govern stem cell renewal in mice (81–86). Although they were identified by the TGMI algorithm, their frequencies of interactions with pathway genes were relatively low (Figure 7A). A possible explanation is that these three master regulators are located at higher hierarchical levels, and are relatively distal from the lower hierarchical pathway genes used to identify them. ROC curves were used to compare the accuracy of TGMI with those of three other existing algorithms using all the three mouse datasets, namely, Dataset 1, 2 and 3. The results indicated that TGMI algorithm had a higher accuracy than the other three algorithms when tested with all three datasets (Figure 7B). The AUROCs of the TGMI algorithm for identifying the pluripotency pathway regulatory TFs using Datasets 1, 2 and 3 were 0.77, 0.79 and 0.80, respectively. Note that the performance of the BWERF and Bottom-up GGM algorithms is based on only one layer of TFs, but these algorithms were designed and tailored to build ML-hGRNs.

Cell cycle pathway in S. cerevisiae

We predicted the pathway regulators that govern cell cycle pathway in yeast. The resulting rankings of TFs are provided in the Supplementary Table S1. ROC curves and AUROCs of TGMI and three other comparative algorithms, BWERF, Bottom-up GGM and ARACNE, were enclosed in the Supplementary Figure S1. Obviously, TGMI had the highest sensitivity/specificity among all methods and AUROCs for TGMI, Bottom-up GGM, BWERF and ARACNE were 0.91, 0.72, 0.71 and 0.5, respectively.

DISCUSSION

The TGMI algorithm was developed for identifying novel regulators that control pathways and biological processes. The underlying principle includes: (i) dissection of the interactions among triple gene block into multiple compo-
Figure 7. Regulatory network for mouse pluripotency maintenance non-canonical pathway built with TGMI and comparison of TGMI with other algorithms. (A) Regulatory network generated using Dataset 3 (335 TF). The green nodes are pathway genes, and all others are TFs. The light coral colored nodes represent known authentic TFs. (B) The performance of TGMI in comparison with those of three other algorithms in identifying mouse pluripotency pathway authentic regulatory TFs. Left: ROC curves generated using 135 TF dataset (Dataset 1). Middle: ROC curves generated using 235 TF dataset (Dataset 2). Right: ROC curves generated using 335 TF dataset (Dataset 3). AUROC was also calculated and provided for comparing the accuracies of different algorithms.

- nents using conditional mutual information; (ii) use of a novel MIM to identify significantly interacted triple genes; (iii) ranking TFs present in the significantly interacted triple genes based on their interference frequency with pathway genes. When testing with four pathways from three species, the TGMI algorithm consistently performed well in identifying true pathway regulators through constructing two-layered regulatory networks with TFs being operating immediately above pathway genes. In addition, TGMI was able to yield combinatorial TFs that co-regulated several of specific lignin pathway genes. TGMI algorithm is based on use of mutual information and conditional mutual information, which have several advantages over linear pairwise association methods (39) because they can be generalized to identify both linear and non-linear relationships (87). As conditional mutual information was introduced and applied to triple gene blocks, more causal relationships could be captured. This is because the evaluation of trivariate variables is better than evaluation of pairwise variables for recognizing causal relationships (45,88,89). The implementa-
tion of TGMI algorithm to four pathways and five datasets obtained from different species demonstrated that TGMI performed better than Bottom-up GGM algorithm, which uses the difference between correlation and partial correlation to identify causal relationships among triple genes. TGMI algorithm enables the emergence of more true regulators by using conditional mutual information on the same triple gene model, and especially the MIM, which was evidenced to serve as a powerful filter to eliminate non-authentic regulatory relationships. To test whether the MIM was most efficient in capturing the authentic regulatory interactions by evaluating triple gene blocks, we also evaluated MIM together with several derivative candidate measures that could also reflect the magnitudes of the interactions within triple gene blocks. The results are shown in Figure 8.

The results, as shown in Figure 8A–D, consistently supported that MIM is the best filter for capturing authentic pathway regulators. We created a training dataset and a test dataset from each of the two Arabidopsis datasets and three mouse datasets. Each training dataset and test dataset contained 75% and 25% randomly drawn rows of all triple gene blocks in each of the five datasets. For each triple gene block, 1 was assigned if the TF was a positive TF, 0 otherwise. Each training dataset was used to build a logistic regression classification model, which was then used to predict the positive TFs in the respective testing data. The prediction performance was measured by determining the ROC AUROCs for the four different triple gene interaction measures plus a random predictor. The results were shown in Figure 8, which indicated that MIM consistently exhibited the best prediction performance among the four interaction measures, and thus could be used to capture positive pathway regulators by evaluating triple gene blocks. The distinct differences between the AUROCs of the four different measures suggest that MIM indeed contributed greatly to identification of positive pathway regulators.

CONCLUSION

We developed a novel and efficient algorithm called TGMI which could generate a regulatory layer operating above a metabolic pathway or biological process for facilitating identification of important regulators that govern various pathways or biological processes. In addition, TGMI algorithm could yield some combinatorial TFs that collectively regulate each individual pathway gene, enabling more precise genetic engineering of regulators that regulate rate-limited steps in a pathway or biological process. The algorithm accomplishes these objectives through dissecting all interaction components among triple gene blocks, each containing two pathway genes and one TF, using conditional mutual information, and then through extracting and summarizing regulatory edges from significantly interacted triple gene blocks identified with MIM. The algorithm was validated with four pathways from plants, ani-
mals and yeast, and the results consistently supported that TGMI was highly effective in capturing true pathway regulators. Performance tests using ROC curves and AUROC values also showed that MIM consistently outperformed several other candidate measures, manifesting MIM’s critical role in bringing the true pathway regulators to light. Since TGMI algorithm does not require time-course data, it is widely applicable to the high-throughput data yielded from treatment versus control or large time-interval time course microarray or RNA-seq experiments, which are most frequently conducted in modern genomics. We thus think TGMI can meet the great needs of the biological research community in identifying pathway regulators for more efficient genetic modification of various metabolic pathways and biological processes.

DATA AVAILABILITY

The R package for TGMI is freely available at: http://sys.bio.mtu.edu/sample_output/TGMI/

SUPPLEMENTARY DATA

Supplementary Data are available at NAR Online.

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