Genomic prediction models for traits differing in heritability for soybean, rice, and maize

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Abstract
Background: Genomic selection is a powerful tool in plant breeding. By building a prediction model using a training set with markers and phenotypes, genomic estimated breeding values (GEBVs) can be used as predictions of breeding values in a target set with only genotype data. There is, however, limited information on how prediction accuracy of genomic prediction can be optimized. The objective of this study was to evaluate the performance of 11 genomic prediction models across species in terms of prediction accuracy for two traits with different heritabilities using several subsets of markers and training population proportions. Species studied were maize (Zea mays, L.), soybean (Glycine max, L.), and rice (Oryza sativa, L.), which vary in linkage disequilibrium (LD) decay rates and have contrasting genetic architectures.

Results: Correlations between observed and predicted GEBVs were determined via cross validation for three training-to-testing proportions (90:10, 70:30, and 50:50). Maize, which has the shortest extent of LD, showed the highest prediction accuracy. Amongst all the models tested, Bayes B performed better than or equal to all other models for each trait in all the three crops. Traits with higher broad-sense and narrow-sense heritabilities were associated with higher prediction accuracy. When subsets of markers were selected based on LD, the accuracy was similar to that observed from the complete set of markers. However, prediction accuracies were significantly improved when using a subset of total markers that were significant at $P \leq 0.05$ or $P \leq 0.10$. As expected, exclusion of QTL-associated markers in the model reduced prediction accuracy. Prediction accuracy varied among different training population proportions.

Conclusions: We conclude that prediction accuracy for genomic selection can be improved by using the Bayes B model with a subset of significant markers and by selecting the training population based on narrow sense heritability.

Keywords: Maize (Zea mays L.), Soybean (Glycine max L.), Rice (Oryza sativa L.), Genomic selection/prediction, Bayes B, Genomic estimated breeding values

Background
Plant breeders observe the phenotypes of crops to choose desirable offspring in an aim to genetically improve target traits. Selection during the breeding process is a crucial step in crop breeding, with historical and current conventional plant breeding depending on phenotypic selection. The Selection-index (SI) method [1] selects multiple traits simultaneously based on a total score, is
more efficient than selection for one trait at a time, and
can improve aggregate genetic gain over time [2]. With
advancements in computation, Henderson [3] proposed
the best linear unbiased prediction (BLUP), which has
become the most widely used method for genetic evalua-
tion. High throughput genotyping methods have resulted
in a large number of molecular markers that are avail-
able to assist in crop breeding. Although marker-assisted
selection (MAS) is a popular method in molecular crop
breeding [4], utilization of MAS has been limited in
breeding programs because many of the important agro-
monic traits in crop breeding are complex and controlled
by a large number of genes with small effects [5], making
effective MAS difficult or impossible.

Genomic selection provides a potential advantage in
crop breeding by accelerating the genetic improvement
of crops per unit time through the reduction in cost per
breeding cycle and shortening of the generation interval [6]. Additionally, genomic prediction can save labor
costs compared to conventional breeding [7]. Meuwis-
sen et al. [8] proposed a genomic selection method that
uses genome-wide markers to estimate the effects of
all loci and from which a genomic estimated breeding
value (GEBV) can be computed to make the prediction
for progeny of the target set with only genotypic data. A
basic requirement for genomic prediction is that mark-
ers are distributed throughout the genome so that at least
one marker is in linkage disequilibrium (LD) with each
QTL [9]. All markers are used simultaneously to esti-
mate effects using a “training” population [10]. Based on
the training population, genomic prediction can predict
GEBVs of individuals for selection. The GEBV of each
individual can be estimated using markers whose effects
can be estimated using a linear mixed model of the form
\[ y = X\beta + Z\alpha + e \]
where \( y \) is a vector of standardized pheno-
types, \( \beta \) is a vector of fixed effects, \( \alpha \) is a vector of ran-
dom effects for each marker, \( e \) is the random error, and
\( X \) and \( Z \) are incidence matrices. When the number of
predictors (markers) is much higher than the number of
genotypes, fixed regression methods using ordinary least
squares cannot be used for developing prediction models
because of overfitting among predictors [11].

Numerous genomic prediction models have been
developed for predicting phenotypes using large sets of
genetic markers (relevant examples are listed in Addi-
tional File 1, Table S1). Variation resulting from hun-
dreds or thousands of markers can be controlled by
various shrinkage and variable selection methods. Mod-
els differ in various assumptions including the distribu-
tion of marker effects and marker variances. Methods
such as ridge regression assume that marker effects are
homogeneously distributed across the genome [12],
whereas Bayesian methods allow for heterogeneity
among markers, with some markers having effects com-
ing from a different underlying distribution than others
[13]. In methods such as BayesB, a prior probability dis-
tribution is used to select a proportion of markers with
non-zero effects; in least absolute shrinkage and selection
operator (LASSO) models, penalties are used to select
markers with major effects [14]. BayesB and Bayesian
LASSO methods can identify a subset of markers with
large effects (variable selection) and use them for making
predictions.

The utility of genomic prediction is expressed as the
correlation between predicted and phenotypic values so
that prediction of the individuals can be made accurately
in earlier generations, with the aim to shorten selection
cycles. Generally, it is assumed that the accuracy of pre-
diction can be increased as more individuals are included
in the training population and more markers are used
in the prediction model. However, in practice this is not
true in every case; increased size of the training popula-
tion and increased number of markers in the prediction
model may not lead to improved prediction accuracy
(PA) [15] because of overfitting or due to the presence
of non-informative individuals in a larger training popu-
lation. Therefore, the first step in genomic prediction
is to determine the size of the training population and
the number of markers used in the appropriate predic-
tion model to estimate the GEBVs with an aim to obtain
high predictive ability. The second step is the validation
and testing of the models to predict the phenotype of
those lines that were not present in the training models
[16]. The accuracy of a model for prediction is typically
evaluated using cross-validation techniques under the
assumption that random partitioning of the data results
in independent training and testing sets [12, 17]. Both
the manner in which training–testing partitions are con-
structed, as well as the level of relatedness among indi-
viduals, have effects on cross validation results [13].

Several factors affect the accuracy of genomic predic-
tion including the size and genetic diversity of the train-
ing population, trait heritability, marker density, gene
or marker effects, and the extent and distribution of LD
between markers and QTL. Therefore, there is an ongo-
ing need to understand how accuracy of different mod-
els reacts among crop species that vary in the LD decay
as well as how prediction accuracy is affected by marker
number, training population proportion, and trait herit-
ability. The main objective of this study was to compare
the accuracy of numerous genomic prediction models
for several traits that differ in heritability for three crop
species with different LD decays rates and contrasting
genetic architecture, as well as testing the effect of sev-
eral methods of sub-setting total marker number and the
interaction with training population size.
Results

Descriptive statistics of phenotypes

Broad sense heritability and descriptive statistics of all traits for soybean [18, 19], maize [20], and rice [21] are presented in Table 1. There was a wide range of phenotypic variation for each trait. In soybean, CW ranged by 38.1% and δ13C ranged by 1.46%. In maize, the DT ranged by 30.5 days and the EH ranged by 128 cm. In rice, the PPP ranged by 1.89 panicles and the SPP ranged by 2.19 seeds (Table 1).

Markers distribution in subsets and narrow sense heritability

Tables S2, S3, and S4 (Additional File 1) show the distribution of markers across all chromosomes in different subsets of markers for all traits for all three crops. The number of markers was highest in maize compared to soybean and rice. To map a given trait with similar accuracy, maize requires a larger number of markers than soybean or rice because of faster LD decay. Both methods that were used to select subsets of markers reduced the marker number. Using subsets of markers based upon haplotype blocks decreased the number of markers by up to 58% (soybean), 26% (maize), and 37% (rice) (Table 2). Using subsets of markers based upon the probability ($P = 0.05$) of the association between a marker and given trait by FarmCPU [22] decreased the number of markers up to 97% (soybean), 96% (maize), and 98% (rice) (Table 2).

Marker based narrow sense heritability was estimated using marker information for all traits in the three crops for all different sets of markers and training population proportions. There was variation in $h^2$ for all traits when using different subsets of markers for different training population proportions (Table 3). In general, for soybean and rice, $h^2$ tended to increase as the subsets of markers based on $P$-values decreased from $P = 0.50$ to 0.05 (Table 3). This response was less evident in maize as $h^2$ was largely unaffected by $P$-value, trait, or training population proportion. There was no discernable impact on $h^2$ of limiting the subset of markers based on LD for any crop at any training population proportion.

Genomic prediction accuracy in soybean, rice, and maize

Prediction accuracy of different genomic prediction models was compared for several traits differing in Table 1. Descriptive statistics and broad sense heritability of canopy wilting (CW) and carbon isotope ratio ($\delta^{13}$C) in soybean, panicles per plant (PPP) and seeds per plant (SPP) in rice, and days to tasseling (DT) and ear height (EH) in maize

| Trait | CW (%) | δ13C (%) | PPP | SPP | DT (days) | EH (cm) |
|-------|--------|----------|-----|-----|-----------|---------|
| Soybean | 16.99 | −29.06 | 3.24 | 4.86 | 67.58 | 61.38 |
| Rice | 6.46 | 0.27 | 0.41 | 0.34 | 5.75 | 20.27 |
| Maize | 45.63 | −28.37 | 4.12 | 5.63 | 85 | 136 |

*a CW data from Kaler et al. [18], and $\delta^{13}$C from Kaler et al. [19]  
*b Data from Zhao et al. [21]  
*c Data from Wallace et al. [20]

Table 2. Marker distribution in the different subsets of markers were selected based on the two methods: (1) when linkage disequilibrium between markers was correlated at $r \geq 0.90$ (LD_90), $r = 0.80$ (LD_80), $r = 0.70$ (LD_70), $r = 0.60$ (LD_60) and (2) when SNP markers were significant with the respective traits at P-values of 50% (SNP_5), 10% (SNP_1), 5% (SNP_05), or non-significant (SNP_NS). The traits evaluated included canopy wilting (CW) and carbon isotope ratio ($\delta^{13}$C) for soybean, panicles per plant (PPP) and seeds per plant (SPP) for rice, and days to tasseling (DT) and ear height (EH) for maize

| Crop | Trait | Complete | LD_90 | LD_80 | LD_70 | LD_60 | LD_50 | SNP_5 | SNP_1 | SNP_05 | SNP_NS |
|-------|-------|----------|-------|-------|-------|-------|-------|-------|-------|-------|--------|
| Soybean | CW | 31,260 | 18,971 | 17,650 | 15,944 | 14,458 | 13,045 | 14,06 | 2111 | 29,138 |
| | δ13C | 31,260 | 18,971 | 17,650 | 15,944 | 14,458 | 13,045 | 14,06 | 2111 | 29,138 |
| Rice | PPP | 34,848 | 28,390 | 26,808 | 25,437 | 23,910 | 22,107 | 2337 | 1043 | 33,804 |
| | SPP | 34,848 | 28,390 | 26,808 | 25,437 | 23,910 | 22,107 | 2337 | 1043 | 33,804 |
| Maize | DT | 48,833 | 42,605 | 40,951 | 39,421 | 37,824 | 36,050 | 4277 | 2070 | 46,763 |
| | EH | 48,833 | 42,605 | 40,951 | 39,421 | 37,824 | 36,050 | 4277 | 2070 | 46,763 |
heritability in soybean, rice, and maize varying in LD decays rates using all markers, as well as several subsets of markers delimited by LD (five threshold subsets) or by marker significance (four threshold subsets) and training-to-testing population proportions. We found a difference in prediction accuracy for all traits in soybean, rice, and maize using different subsets of markers at three training-to-testing proportions (Fig. 1). Comparing different sets of markers, the subset SNP_05 yielded higher accuracy than the complete marker set, subsets selected based on the LD, and non-significant subset for all traits in soybean, rice, and maize.

Because the highest prediction accuracy was when using the SNP_05 subset, this subset was used to compare the different genomic prediction models (Fig. 2). For soybean, BayesB had the highest prediction accuracy for CW and $\delta^{13}$C at all cross-validation levels. For SPP in rice, BayesB yielded the highest accuracy for all cross-validation levels. For PPP in rice, the accuracies of all models were similar for all of proportions between training and testing. For DT in maize, the highest prediction accuracy models were BayesB and RKHS at the 90:10 proportion. At the 70:30 and 50:50 proportions, the accuracies of all these models were mostly similar. For EH in maize, BayesB had the highest prediction accuracy at all training-to-testing proportions.

**Effect of the different training population proportions**

Because a subset of significant markers selected at the significance level of $P < 0.05$ increased prediction accuracy in all selected traits of all crops, this subset was used to report the effect of the different training-to-testing population proportions (Fig. 2). Individuals were randomly assigned to training or testing sets, and this process was repeated 10 times. The effect of different testing population proportions on the prediction accuracy varied for different traits of these crops. For example, prediction accuracy of $\delta^{13}$C and PPP was highest when the testing population proportion was 10% followed by 50 and 30% of the population. For CW, prediction accuracy was highest when the testing population proportion was 30% followed by 10 and 50% of the population. For SPP and EH, prediction accuracy was highest when the testing population proportion was 10% of the population followed by 30

| Traits | TPS (%) | Com | SNP_5 | SNP_1 | SNP_05 | SNP_NS | LD_90 | LD_80 | LD_70 | LD_60 | LD_50 |
|--------|---------|-----|-------|-------|--------|--------|-------|-------|-------|-------|-------|
| Soybean |         |     |       |       |        |        |       |       |       |       |       |
| CW     | 90      | 74  | 76    | 77    | 78     | 76     | 75    | 76    | 76    | 75    | 75    |
|        | 70      | 59  | 71    | 71    | 75     | 71     | 64    | 68    | 69    | 65    | 65    |
|        | 50      | 79  | 79    | 80    | 79     | 79     | 78    | 79    | 79    | 78    | 78    |
| $\delta^{13}$C | 90    | 27  | 36    | 38    | 41     | 36     | 27    | 28    | 28    | 27    | 27    |
|        | 70      | 38  | 46    | 45    | 48     | 46     | 38    | 39    | 39    | 37    | 38    |
|        | 50      | 36  | 43    | 44    | 41     | 43     | 36    | 37    | 37    | 36    | 35    |
| Rice   |         |     |       |       |        |        |       |       |       |       |       |
| SPP    | 90      | 36  | 49    | 51    | 52     | 27     | 27    | 34    | 34    | 33    | 34    |
|        | 70      | 25  | 33    | 38    | 38     | 21     | 21    | 24    | 24    | 25    | 24    |
|        | 50      | 28  | 42    | 38    | 43     | 23     | 23    | 28    | 27    | 26    | 26    |
| PPP    | 90      | 61  | 78    | 81    | 80     | 57     | 57    | 61    | 61    | 61    | 61    |
|        | 70      | 70  | 88    | 88    | 87     | 66     | 66    | 71    | 71    | 71    | 72    |
|        | 50      | 77  | 84    | 82    | 77     | 74     | 74    | 76    | 76    | 76    | 76    |
| Maize  |         |     |       |       |        |        |       |       |       |       |       |
| DT     | 90      | 80  | 85    | 85    | 83     | 76     | 76    | 81    | 80    | 81    | 81    |
|        | 70      | 63  | 69    | 70    | 68     | 60     | 60    | 63    | 63    | 64    | 64    |
|        | 50      | 97  | 99    | 99    | 98     | 88     | 88    | 98    | 98    | 98    | 98    |
| EH     | 90      | 60  | 74    | 79    | 74     | 52     | 52    | 61    | 62    | 62    | 62    |
|        | 70      | 52  | 64    | 63    | 61     | 44     | 44    | 52    | 52    | 53    | 52    |
|        | 50      | 70  | 77    | 79    | 71     | 59     | 59    | 69    | 70    | 69    | 69    |

Table 3 Marker based narrow sense heritability ($h^2$) for canopy wilting (CW) and carbon isotope ratio ($\delta^{13}$C) in soybean, and seeds per plant (SPP) and panicles per plant (PPP) in rice, and days to tasseling (DT) and ear height (EH) in maize using 10 sets of markers in different training-to-testing proportions (TPS)

† Subsets of markers included a complete set (Com), SNP markers significant at $P$-values of 0.50 (SNP_5), 0.10 (SNP_1), 0.05 (SNP_05) or based upon linkage disequilibrium when the correlation coefficient between markers in a LD block were $\geq 0.90$ (LD_90), 0.80 (LD_80), 0.70 (LD_70), 0.60 (LD_60), or 0.50 (LD_50)
and 50% of the population. For DT, prediction accuracy was highest when the testing population proportion was 30% followed by 50 and 10% of the population. These trends were similar for all the different sets of marker subsets (based upon significance threshold levels or LD decay rate; Additional File 1, Tables S6, S7, S8).

Effect of marker density among species and traits on prediction accuracy
The effect of marker density is reported using BayesB model for each trait from each crop species including wilting (CW) in soybean, seeds per plant (SPP) in rice, and ear height (EH) in maize at the 90:10 training-to-testing proportion (Fig. 3). We used Bayes B model because it had a higher prediction accuracy than other models and had a lower computational requirement. There was no increase in accuracy among the non-significant subset of markers and marker subsets delimited by LD (five threshold subsets) among crop species compared with the full set of markers. When subsets of markers were selected based on significance, prediction accuracy was increased for all traits among species. Significant markers selected at the significance level of $P < 0.1$ and $P < 0.05$ had the highest prediction accuracy for all selected traits for all crops. Significant markers at $P < 0.05$ had the highest prediction accuracy for all traits except for DT at 50:50 proportion, where significant markers at $P < 0.1$ had the highest prediction accuracy.

Effect of narrow sense heritability on prediction accuracy
We estimated $h^2$ for all traits using all the different combinations of markers sets and three training-to-testing
proportions (90:10, 70:30, and 50:50). (Table 3). We observed strong to moderate positive correlations between $h^2$ and prediction accuracy of models under different sets of markers for all traits for all training population proportions (Additional File 1, Table S5). The effect of subsets of markers on $h^2$ followed the same trend as the effect on the prediction accuracies.

**Discussion**

This study evaluated the prediction accuracy of different genomic prediction models for crop species differing in LD and marker density, for traits differing in heritability, differences in marker density, and how proportions in the training-to-testing population affected prediction accuracy. To build a genomic prediction model, there is a need for a wide phenotypic variation [10], which was observed in this study. A basic assumption in genomic selection is that markers are distributed throughout the genome to provide sufficient coverage such that at least one marker is in LD with QTL that control the phenotypic variation. Genomic prediction models use all those effects to estimate GEBVs for progeny of the same or future generations [23].

We found that maize and rice had higher prediction accuracies than soybean. These crop species had different levels of LD/LD decay, which plays an important role in identifying marker-QTL associations [24]. Maize has a faster LD decay over physical distance compared to rice and soybean [18, 19, 25, 26]. Both maize and rice had more markers scattered over the genome than soybean, which increases the probability of having at least one marker in LD with a QTL [27]. The smaller number of markers with large effects in soybean may not explain all the genetic variance or may fail to capture small effect QTLs [28, 29]. Thavamanikumar et al. [30] reported similar results of difference in prediction accuracy among wheat populations varying in LD decay, which indicated that a high LD decay rate increases prediction accuracy.

In comparing the subsets of markers selected based on different LD levels and significance levels, we found there was a similar prediction accuracy for a complete set and subsets of markers selected based on LD. Thus, a haplotype block performed similar to a single marker. Adding more random markers in these conditions did not improve accuracy but may have increased error or noise. Poland et al. [31] and Spindel et al. [32] evaluated random subsets of markers and observed no change in accuracy. Prediction accuracies were increased when markers were selected that had some association with the phenotype instead of using all markers that may have created noise or error. In addition to subsets of
markers evaluated at $P$-values of 0.05, 0.10, and 0.50, we also compared the effect of marker density of subsets of markers selected at 13 different levels of significance on prediction accuracy (Additional File 2, Fig. S1). Prediction accuracy increased as the significance level of markers decreased until $P < 0.05$, but there was no further increase in accuracy at lower $P$ values. We conclude that significant markers should be selected up to a probability/significance level where they still have adequate genomic coverage. These results are consistent with previous research [30] in which there was greater accuracy when using QTL-linked markers than when using a random set of markers. The importance of including markers identified from QTL and association studies in prediction models was demonstrated when the QTL-linked markers were excluded from the models and there was a lower accuracy compared to other sets of markers [30].

As expected, higher prediction accuracies were observed for high heritability traits compared to low heritability traits. Similar results were observed in other studies where there was a strong relationship between prediction accuracy and trait heritability [27, 33–35]. Similar to broad-sense heritability, marker based narrow sense heritability varied among the traits in this study. There were strong positive correlations between marker based narrow sense heritability and prediction accuracy for all traits for all training-to-testing population proportions, indicating that marker based narrow sense heritability might be associated with prediction accuracy. Similar to accuracy, subsets of markers selected based on the different significance levels increased marker based narrow sense heritability, but LD based subsets of markers did not. Extra markers might be associated with an increase in error or noise from LD based subsets. We conclude that selecting training population proportions based on marker based narrow sense heritability may generally improve prediction accuracy.

Among all models, BayesB performed better than or equal to all other models, for all traits in all three crop species. The BayesB model performs both shrinkage and variable selection on markers included in the model [36]. In the BayesB model, the prior probability of a marker
having a non-null effect ($\pi$) was set at 0.05, which might be associated with higher predictive ability values compared to higher prior setting. Results from this study agree with other studies, indicating that selecting a model that performs specific shrinkage and variable selection would improve prediction accuracy. For example, Bayesian Lasso and BayesB share some characteristics, and these models performed better than GBLUP, which assumes equal variance for each marker [23, 27].

The better performance of BayesB over other models was highly dependent on the presence of large QTL effects, which was demonstrated by Daetwyler et al. [14] through simulations. Several studies reported the better performance of BayesB over all models in genomic prediction of traits that are controlled by a few loci with large effects [14, 37, 38]. Habier et al. [24] provided another comparison between BayesB and rrBLUP models, indicating that BayesB uses LD between markers and QTL in making predictions, where RR-BLUP mainly captures the genetic relationships. Accuracies of the models using LD between markers and QTL persist for several generations, whereas accuracies of the models using genetic relationships decay over generations [24].

In this study, prediction accuracy was affected more by LD between the markers and QTLs than the genetic relationships. The effect of different training population proportions on prediction accuracy was compared in this study for all traits in three crops by randomly repeating the simulations 10 times. We observed a difference in prediction accuracy among training population proportions that might be due to the random selection of the training population. A random population could have a different genetic diversity or population structure, which could have different marker-QTL associations or marker effect sizes. Similar results of varied prediction accuracies due to different training populations were observed in other studies [39]. Charmet et al. [40] observed that predicted accuracy was not improved with an increase of the training population proportion. However, de Azevedo Peixoto et al. [41] observed an increase in prediction accuracy when the training population proportion increased.

**Conclusions**

In this study, we compared the prediction accuracy of different genomic prediction models for several traits differing in heritability in three crops varying in LD decays rates with contrasting genetic architecture using several subsets of markers and training population proportions. Among all models, BayesB performed better than or equally well as all other models for all traits in three crop species. Higher prediction accuracy was observed in maize with a faster LD decay compared to slower LD decay in soybean and rice. Traits with higher broad or narrow sense heritability had higher prediction accuracy. Instead of using a complete set of markers, selecting subsets of markers based on the significance level increased prediction accuracy. Prediction accuracy was greatest for all crops when using a subset of markers that were significant at $P \leq 0.05$. In contrast, subsets of markers selected based on the LD level did not show any change in the accuracy. Different training population proportions varied prediction accuracy for all traits in three crops.

**Materials and methods**

**Plant materials and phenotypic traits**

Data sets for three plant species that vary in LD decay rates were selected for our experiments: soybean (*Glycine max* L.), maize (*Zea mays* L.), and rice (*Oryza sativa* L.). For each crop, two traits were used that varied in broad-sense heritability ($H^2$). For soybean, these traits included canopy wilting (CW, $H^2 = 80\%$, [19]) and carbon isotope ratio ($\delta^{13}$C, $H^2 = 60\%$, [18]). For maize, traits evaluated were days to tasseling (DT, $H^2 = 85\%$) and ear height (EH, $H^2 = 65\%$) [20]. Lastly for rice, we evaluated panicles per plant (PPP, $H^2 = 80\%$) and seeds per plant (SPP, $H^2 = 55\%$) [21].

Soybean data consisted of 346 accessions that were used for association mapping of CW [19] and $\delta^{13}$C [18]. Rice data consisted of 352 accessions that were obtained from the rice diversity database [21]. Maize data consisted of 279 accessions that were obtained from the Panzea database website [20]. Both maize (https://www.panzea.org/data) and rice data (http://ricediversity.org/data/) were publicly available and soybean data are included herein (Additional file 3).

**Genotypic data**

For all three crops, genotypic data were comprised of single nucleotide polymorphisms (SNPs). In soybean, SNP data were obtained using the application of Illumina Infinium SoySNP50K iSelect SNP BeadChip that provided 42,509 SNPs for all 346 accessions ([42, 43], and datasets supporting the conclusions of this article are included within the article (Additional Files 3 and 4).

Additional file 3). In maize, SNP data were obtained using the application of Illumina MaizeSNP50 BeadChip that provided 50,896 SNPs for all 273 accessions [20]. In rice, SNP data of 44,100 markers were obtained from two projects: *Oryza*SNP project, an oligomer array-based re-sequencing effort using Perlegen Sciences technology and BAC clone Sanger sequencing of wild species from OMAP project [21]. Quality control checks for the three species consisted of eliminating
monomorphic markers, markers with minor allele frequency (MAF) ≤ 5%, and markers with a missing rate higher than 10%. Remaining marker datasets were imputed using an LD-kNNi method, which is based on a k-nearest-neighbor-genotype [44]. The final complete SNP marker datasets consisted of 31,260 SNPs for soybean, 48,833 SNPs for maize, and 34,848 SNPs for rice. A pairwise SNP LD decay among the markers for these crops was estimated, which indicated that the decay of LD to r² = 0.25 level was much faster in maize (1 kb) than soybean (150 kb in euchromatic and 5 kb in heterochromatic regions) or rice (123 kb).

Genomic prediction models
Eleven different statistical models were compared for genomic predictions. These models differ with respect to assumptions about the markers as described in Additional File 1, Table S1. Prediction models were tested using different packages including sommer, rrBLUP, BGLR, plyr, MCMCglmm, EMMREML, and BLR in the R program.

Testing subsets of markers in prediction models
Ten different marker subsets were compared to evaluate the effects of marker distribution across the genome on the prediction accuracy. Subsetting markers was done based on two approaches: 1) linkage disequilibrium between markers and 2) markers that met a significance threshold. Linkage disequilibrium between markers, which defines a haplotype block, was evaluated using the correlation coefficient between alleles at a pair of genetic loci. Five LD based subsets of markers were selected from the haplotype block that was made using a correlation coefficient (r) of r ≥ 0.90, 0.80 ≤ r < 0.90, 0.70 ≤ r < 0.80, 0.60 ≤ r < 0.70, and 0.50 ≤ r < 0.60 between alleles. For simplicity, these subsets are subsequently referred to as 0.90, 0.80, 0.70, 0.60, and 0.50, respectively. For example, if a haplotype block consisted of five SNPs that were linked with each other at r ≥ 0.90, then only one SNP out of five was kept in the subset of markers.

In addition to selecting marker subsets based upon haplotype blocks, we also selected subsets of markers based on the P-value of the significant association of markers with a trait at probability levels of P < 0.5 (SNP_5), P < 0.1 (SNP_1), and P < 0.05 (SNP_05). The significant association between markers and traits was conducted using the Fixed and random model Circulating Probability Unification (FarmCPU) model [22]. One subset of markers consisted of non-significant SNP markers at P > 0.05 (SNP_NS). The F-test for two-samples of variance was conducted to compare the significant effect between the different sets of markers.

Testing the size of the training population and model validation
Three different sizes of training populations among these species were evaluated to determine the effect of the training population proportion on the genomic prediction accuracy. These three training population proportions consisted of 90 training to 10 testing set, 70 training to 30 testing set, and 50 training to 50 testing set. Random assignments of individuals to training and testing sets were repeated 10 times and the average value of the prediction accuracy are reported in this work. The correlation coefficient (r) between the GEBVs and observed phenotypic values was used to determines predictive ability (r), which was used as the indicator of prediction accuracy in this paper. This approach has been used previously by several groups [45, 46].

Estimation of narrow sense heritability
Marker-based narrow sense heritability (h²) was estimated to understand the variation and trend of predictive ability across traits [47] using the GAPIT R package. In the GAPIT package, the MLM model can be described as follows: $Y = X\beta + Zu + e$, where Y is the vector of observed phenotypes; $\beta$ is an unknown vector containing fixed effects, including the genetic marker, population structure (Q), and the intercept; u is an unknown vector of random additive genetic effects from multiple background QTLs for individuals/lines; X and Z are the known design matrices; and e is the unobserved vector of residuals. The u and e vectors are assumed to be normally distributed with a null mean and a variance of: $\text{Var} \left( \begin{array}{c} u \\ e \end{array} \right) = \left( \begin{array}{c} G \\ 0 \\ 0 \\ R \end{array} \right)$, where G = $\sigma^2_aK$ with $\sigma^2_a$ as the additive genetic variance and K as the kinship matrix. Homogeneous variance was assumed for the residual effect (i.e., R = $\sigma^2_eI$, where $\sigma^2_e$ is the residual variance). The proportion of the total variance explained by the genetic variance is defined as marker-based narrow sense heritability, which was calculated for all traits using different subsets of markers and different training-to-testing population proportions.

**Abbreviations**
- QTL: Quantitative trait locus/loci
- LD: Linkage disequilibrium
- SNP: Single nucleotide polymorphism
- GEBV: Genomic estimated breeding value
- BLUP: Best linear unbiased prediction
- MAS: Marker-assisted selection
- LASSO: Least absolute shrinkage and selection operator
- PA: Prediction accuracy
- CW: Canopy wilting
- 613C: Carbon isotope ratio (δ13C)
- PPP: Panicles per plant
- SPP: Seeds per plant
- DT: Days to tasseling
- EH: Ear height
Supplementary Information

The online version contains supplementary material available at https://doi.org/10.1186/s12870-022-03479-y.

Additional file 1: Table S1. Main features of thirteen genomic prediction models. Table S2. Markers distribution in the different subsets of markers, which were selected based on the two methods, linkage disequilibrium (LD) between markers and significant markers, in soybean for two traits including canopy wilting (CW) and carbon isotope ratio ($\delta^{13}$C). Table S3. Markers distribution in the different subsets of markers, which were selected based on the two methods, linkage disequilibrium (LD) between markers and significant markers, in maize for two traits including days to tasseling (DT) and ear height (EH). Table S4. Markers distribution in the different subsets of markers, which were selected based on the two methods, linkage disequilibrium (LD) between markers and significant markers, in rice for two traits including panicles per plant (PPP) and seeds per plant (SPP). Table S5. Correlations of narrow sense heritabilities and prediction accuracies of 11 different genomic prediction models for canopy wilting (CW) carbon isotope ratio ($\delta^{13}$C), seeds per plant (SPP), panicles per plant (PPP), and days to tasseling (DT) and ear height (EH) at different training-to-testing proportions (90/10%, 70/30%, & 50/50%). Table S6. Prediction accuracy of genomic models for canopy wilting (CW) and carbon isotope ratio ($\delta^{13}$C) in soybean, and seeds per plant (SPP) and panicles per plant (PPP) in rice, and days to tasseling (DT) and ear height (EH) in maize using different subsets of markers at the 90/10% training-to-testing proportion. Table S7. Prediction accuracy of genomic models for canopy wilting (CW) and carbon isotope ratio ($\delta^{13}$C) in soybean, and seeds per plant (SPP) and panicles per plant (PPP) in rice, and days to tasseling (DT) and ear height (EH) in maize using different subsets of markers at the 70/30% training-to-testing proportion. Table S8. Prediction accuracy of genomic models for canopy wilting (CW) and carbon isotope ratio ($\delta^{13}$C) in soybean, and seeds per plant (SPP) and panicles per plant (PPP) in rice, and days to tasseling (DT) and ear height (EH) in maize using different subsets of markers at the 50/50% training-to-testing proportion.

Additional file 2: Fig. S1. Prediction accuracies for carbon isotope ratio ($\delta^{13}$C) in soybean using BayesB model and a training-to-testing cross-validation proportion of 90:10%. Thirteen sets of marker subsets were selected based on the different significant levels including $P < 0.001$, $P < 0.0025$, $P < 0.005$, $P < 0.0075$, $P < 0.01$, $P < 0.025$, $P < 0.05$, $P < 0.075$, $P < 0.1$, $P < 0.25$, $P < 0.5$, $P < 0.75$, and complete set.

Additional file 3. Zip file containing genotypic and phenotypic data files for three datasets: soybean, two traits ($\delta^{13}$C and CW) and 42,509 SNPs for 346 accessions, maize, two traits (DT and EH) and 50,896 SNPs for 273 accessions, rice, two traits (PPP and SPP) and 44,100 markers from two projects: OryzaSNP project and OMAP project.

Additional file 4. Zip file containing R scripts used in this study.

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Authors’ contributions

AK wrote initial draft of the manuscript, and was primarily responsible for data analysis. JDG and TB contributed towards data evaluation and presentation. JDG and LP coordinated and supervised the project. All authors were involved in writing and editing and read and approved the final manuscript.

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Availability of data and materials

All data analyzed during this study are included in this published article in are available in Additional file 3. Scripts used in our analyses are available in Additional file 4.

Declarations

Ethics approval and consent to participate

Not applicable. This study complies with all relevant local and national regulations.

Consent for publication

Not applicable.

Competing interests

Not applicable.

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