Dynamic Support Stiffness of Motorized Spindle Bearings under High-speed Rotation

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Dynamic Support Stiffness of Motorized Spindle Bearings under High-speed Rotation

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ABSTRACT: The rotor operating stiffness of high-speed motorized spindles (HSMSs) is key to machining accuracy. Because HSMSs are difficult to load due to their high speeds, a contact loading device was developed to test rotor operating stiffness. The dynamic support stiffness of the front/rear bearings (DSSB) is the main factor affecting the rotor operating stiffness. Two novel experimental schemes for measuring the DSSB are proposed: 1) indirect measurement—by analysing deformation displacements at two points on the external loading rod of the HSMS, and 2) direct measurement—by eddy current sensors installed near the front/rear bearings. Based on the experimental device and two experimental schemes, the influences of working-condition parameters on the DSSB were tested. The results show that the proposed experimental device and two experimental schemes can effectively and accurately measure rotor operating stiffness and DSSB at speeds of up to 30,000 rpm. However, because the tapered connection gap between the loading rod and rotor increases the measured deformation displacement, the DSSB measured by the indirect measurement scheme was relatively small. The DSSB decreases with speed and increases with radial force and working temperature. This study provides a new experimental basis for the quality inspection of finished HSMSs and the verification of theoretical bearing stiffness models.

Keywords: High-speed motorized spindle, bearings, high-speed loading, dynamic support stiffness

1. Introduction

Because of its high efficiency, high precision and low energy consumption, high-speed machining technology has become a development trend in modern manufacturing technology\textsuperscript{1}. A high-speed motorized spindle (HSMS) is the basis for high-speed machining technology\textsuperscript{1}. The development of higher speeds and power has meant that the dynamic performance of HSMS has stricter requirements, especially in terms of rotor operating stiffness, which affects machining accuracy, reliability and production efficiency. The rotor operating stiffness of HSMS mainly depends on the dynamic support stiffness of the front/rear bearings (DSSB). However, due to centrifugal force and other inertial effects, the DSSB at high speed changes significantly compared with that at low speed. This directly affects the corresponding dynamic performance of bearing-rotor systems\textsuperscript{2}. Research on experimentally measuring the rotor operating stiffness and DSSB is key to improving the anti-deformation ability of HSMS at high speeds.

The rotor operating stiffness of the HSMS in the rotating state can accurately reflect its anti-deformation
ability in the actual working state. When measuring the rotor operating stiffness or DSSB, the HSMS must first be 
dynamically loaded. However, due to their structural features and high speeds, HSMSs are difficult to dynamically 
load. Existing loading methods can be categorised into contact loading and non-contact loading. Contact loading 
makes the inner ring of a rolling bearing rotate with the rotor of the HSMS, and then loads the stationary outer ring 
of the bearing to achieve loading of the rotor. For example, CHAO et al.³ designed an HSMS reliability test 
platform that uses an electro-hydraulic servo system to load the outer ring of the bearing. ALBRECHT et al.⁴ and 
OZTURK et al.⁵ used impact hammering on the outer rings of bearings. Contact loading is unsuitable for 
high-speed and long-term loading of HSMSs due to serious temperature increases and the wearing of rolling 
bearings at high speeds. Non-contact loading mainly includes electromagnetic loading and hydrostatic gas film 
loading. WANG et al.⁶ and MATSUBARA et al.⁷ designed an electromagnetic loading device, while FENG et al.⁸ 
presented a hydrostatic gas film loading device to measure the stiffness of HSMSs. However, electromagnetic 
loading tends to induce eddy currents, which cause the temperature of the HSMS to rise. In addition, the direction 
of the induced eddy currents is opposite to that of the electromagnetic field, so the higher the rotating speed, the 
lower the electromagnetic loading force. With hydrostatic gas film loading, the air gap must be controlled at about 
ten micrometres, which imposes strict requirements on the machining accuracy and installation accuracy of related 
parts. Additionally, gap adjustment is difficult in non-contact loading and the load is small and eccentric. In 
summary, HSMS dynamic loading methods require improvement.

Loading methods exist to measure the rotor operating stiffness of HSMS; however, there are relatively few 
studies on the direct and quantitative measurement of the DSSB of HSMS. At present, research on the DSSB is 
mainly based on the theoretical analysis of quasi-static⁹ or quasi-dynamic¹⁰ models of bearings; or uses rotor 
dynamics theory to analyse the modal characteristics of bearing-rotor systems¹¹. Experimental methods mainly 
measure the modal characteristics (critical speed or natural frequency, etc.) of the bearing-rotor system to indirectly 
and qualitatively analyse the DSSB¹², ¹³. Sometimes, the above-mentioned contact loading method is used to 
measure the dynamic support stiffness of an external bearing driven by an HSMS. For example, LIN and JIANG¹⁴ 
used the contact loading method to measure the dynamic support stiffness of tandem-duplex angular-contact ball 
bearings driven by an HSMS. There is a lack of experimental methods that can quantitatively measure the DSSB of 
an HSMS under actual working conditions. This is essential for the verification of bearing stiffness models and 
HSMS dynamic performance detection.

By examining the problem of high-speed dynamic loading, this paper designed a method of applying load by 
contacting the outer ring of the rolling bearing with the rotor of the HSMS. This can be used for the stiffness test of 
the HSMS when the speed is as high as 30,000 rpm. To examine the problem of testing the DSSB, an experimental 
scheme was proposed to indirectly measure the DSSB by analyzing the deformation displacement of two points on 
the external loading rod of the HSMS. A special HSMS with eddy current sensors installed near the front and rear 
bearings was designed, which could directly and accurately measure the DSSB and verify the previous
2 Measurement methods of the DSSB
2.1 Experimental HSMS and its equivalent model

The structure of a specially designed HSMS is shown in Figure 1. The main feature of this HSMS is that mounting holes (where eddy current sensors can be installed on the housing near the front and rear bearing positions) are reserved to measure the deformation displacement of the rotor inside the HSMS. Temperature sensors (PT100) are installed on the front and rear bearing seats. The temperature sensor is close to the outer rings of the front and rear bearings and can measure their temperatures in real time. Therefore, the specially designed HSMS can be used to measure the DSSB, as well as the effect of working temperature on the DSSB. In addition, a standard loading rod is installed at the output end of the HSMS in a similar manner to the installation of a cutter, which can be used for radial force loading and external rotor deformation displacement measurement.

To indirectly analyse the DSSB by measuring the loading force and deformation displacement of the rotor, an equivalent model of an HSMS needs to be established, as shown in Figure 1. The support reaction point of the single-row angular contact ball bearings is the pressure centre of the bearing\(^*\). The pressure centre of the
Double-row angular contact ball bearings is located at the midpoint of the pressure centre of the two single-row bearings. The front and rear bearings of the experimental HSMS can be regarded as a double-row bearing, so the supporting reaction points of the front/rear bearings of the experimental HSMS can be illustrated as points A and point B in Figure 1, which are at the midpoint of the pressure centres of the two single-row bearings. The position where the radial force acts is named point D. The positions measured by the four eddy current sensors are named points C, E, F and G.

As shown in Figure 1, segments AB and BE in the equivalent model are beam elements and the front and rear bearings are simplified into a spring. The stiffnesses of the bearings are represented by the stiffness of the springs. The dotted line represents the deflection curve of the rotor under the action of radial load \( F_r \). At this time, it is assumed that the support bearing is rigid and there is no radial displacement deformation\(^{16}\) and the bending deformations at points C and E are represented by \( y_{CB} \) and \( y_{EB} \), respectively. The dot-dash line indicates the displacement curve of the rotor due to the elastic support of the bearings under the action of the radial force \( F_r \). At this time, it is assumed that the rotor is rigid and there is no bending deformation\(^{16}\), and the displacements at points C and E are represented by \( y_{CE} \) and \( y_{EE} \), respectively.

### 2.2 Analysis method of the DSSB

From the static equilibrium conditions, the support reaction forces at support points A and B can be calculated as:

\[
F_A = \frac{l_{BD}^2}{l_{AB}} F_r \quad (1)
\]
\[
F_B = \left(1 + \frac{l_{BD}^2}{l_{AB}^2}\right) F_r \quad (2)
\]

where \( l_{ij} \) is the distance between support points \( i \) and \( j \) in the equivalent model of the HSMS (mm).

Variables \( \delta_A \) and \( \delta_B \) are the contact deformation displacements at support points A and B. Variables \( \delta_A \) and \( \delta_B \) can be approximately equal to the deformation displacement of points F and G, or their values can be obtained by indirect analysis based on the deformation displacement of points C and E. Based on the material mechanics theory, from the deflection curve of the rotor under the action of external force \( F_r \), the bending deformations at point C (\( y_{CB} \)) and point E (\( y_{CE} \)) are:

\[
y_{CB} = \frac{F_r l_{BC}^2}{6EJ} \left(3l_{BD} - l_{BC}\right) \quad (3)
\]
\[
y_{EB} = \frac{F_r l_{BD}^2}{6EJ} \left(3l_{BE} - l_{BD}\right) \quad (4)
\]

where \( E \) (MPa) is the elastic modulus of the rotor; and \( J \) (mm\(^4\)) is the equivalent moment of inertia of the rotor,
where:

\[ J = \frac{\pi d_v^4}{64} \quad (5) \]

where \( d_v \) (mm) is the equivalent diameter of the step shaft equivalent to the optical shaft, which can be calculated by the following formula:

\[ d_v = \sqrt[4]{\frac{L}{\sum_{i=0}^{n} l_i d_i^4}} \quad (6) \]

where \( d_i \) (mm) and \( l_i \) (mm) are the diameter and length of the \( i^{th} \) stepped shaft, respectively, \( L \) (mm) is the total length of the stepped shaft, and \( n \) is the number of steps of the stepped shaft.

The deformation displacements of point C (\( y_{CE} \)) and point E (\( y_{EE} \)) due to the elastic support of the bearings can be calculated from the geometric relationship of the equivalent model of the HSMS:

\[ y_{CE} = \frac{l_{AC}}{l_{AB}} (\delta_A + \delta_B) - \delta_A \quad (7) \]
\[ y_{EE} = \frac{l_{AE}}{l_{AB}} (\delta_A + \delta_B) - \delta_A \quad (8) \]

The total deformation displacements at point C (\( y_{CT} \)) and point E (\( y_{ET} \)), as measured directly by the eddy current sensors, are:

\[ y_{CT} = y_{CB} + y_{CE} \quad (9) \]
\[ y_{ET} = y_{EB} + y_{EE} \quad (10) \]

Variables \( y_{CE} \) and \( y_{EE} \) can be calculated from Equations (3), (4), (9) and (10), then \( y_{CE} \) and \( y_{EE} \) can be substituted into Formulas (7) and (8) to obtain the contact deformation displacements \( \delta_A \) and \( \delta_B \). The radial loading forces \( F_A \) and \( F_B \) at points A and B can be calculated from Equations (1) and (2). According to the definition of stiffness, the DSSB is:

\[ K_A = \frac{dF_A}{d\delta_A} \quad (11) \]
\[ K_B = \frac{dF_B}{d\delta_B} \quad (12) \]

The above method of analysing the DSSB by measuring the deformation displacements at two points on the external loading rod of the HSMS is called the external measurement method (EMM) in this article. Because there is no need to modify the structure and design of the HSMS, the biggest advantage of EMM is its versatility. To
verify the effectiveness of the EMM, a special HSMS was designed (as shown in Figure 1). The eddy current sensors installed near the front and rear bearings can directly measure the contact deformation displacements $\delta_A$ and $\delta_B$ of the front and rear bearings, and are used to directly obtain the DSSB. This method is called the *internal measurement method* (IMM) in this article. The biggest advantage of IMM is that the measured DSSB is more accurate than that of EMM.

3. Experimental setup

Due to the HSMS’s structural characteristics and extremely high rotational speed, it is difficult to achieve dynamic loading of it. In this paper, a novel contact loading device was designed to test the rotor operating stiffness and DSSB. Figure 2 shows the structure and composition of the contact loading device, which is composed of a mechanical device and a measurement and control device. The mechanical device is mainly composed of a cylinder, floating joint, sliding pillar, sliding base and four rolling bearings. The sliding pillar and the sliding base fixed on the experimental rig constitute a *sliding pair*. The sliding pillar is pushed up by the cylinder, so that the outer rings of the rolling bearings installed on the sliding base contact the rotor of the HSMS to achieve loading. The loading principle is shown in Figure 3. By adjusting the air pressure of the cylinder, the radial loading force can be effectively regulated. To avoid mechanical interference caused by coaxiality errors during installation, a floating joint is used to connect the cylinder and force sensor. Oil–air lubrication not only has a lubricating effect but also takes away much heat via the air, which is used to lubricate and cool the contact position between the rolling bearings and the loading rod.

![Fig 2 Test system for rotor operating stiffness and DSSB of HSMS](image-url)
The main components of the measurement and control device are an electric proportional valve, S-type force sensor, eddy current sensors and data collection device. By adjusting the analogue voltage of the electric proportional valve, the air pressure of the cylinder and the loading force can be adjusted. Four eddy current sensors are used to measure the deformation displacement of the HSMS rotor. The S-type force sensor is used to measure the loading force. The data collection device consists of an N/I Compact DAQ chassis (cDAQ-9174) and computer software. The N/I 9239 module can measure the signal of the sensors simultaneously. The N/I 9263 module can control the analog voltage of the electric proportional valve. The computer software is compiled in LABVIEW language and provides an interface for loading force control and the display, analysis, storage and printing of sensor signals. Finally, the relationship between loading force and deformation displacement is obtained in the computer software, and the rotor operating stiffness and DSSB under high-speed rotation are effectively measured and analysed.

There are some advantages to the HSMS dynamic support stiffness testing system proposed in this paper: 1) Compared with the traditional contact loading techniques described in the Introduction, this test system has lower installation accuracy requirements and has little effect on the dynamic balance of the HSMS rotor, so the applicable speed is higher. Compared with non-contact loading systems, the structure of the test system is simple and the loading force is high and stable. 2) Using at least two eddy current sensors to measure the deformation displacement of the HSMS rotor combined with the experimental data analysis method described in Section 2.2, the DSSB can be quantitatively measured. 3) The loading force can be conveniently and accurately controlled by the electric proportional valve. The loading force and deformation displacement can be measured synchronously in real-time. The measurement accuracy of the testing system is high. 4) The loading rod is installed on the HSMS in a similar way to a cutter, which makes it convenient for testing different types of HSMSs. Hence, the testing system has high versatility.

4. Experimental process and results

4.1 Experimental process

The test system in Figure 2 was used to test the DSSB of the experimental HSMS. Before the experiment, the
minimum proportional valve voltage $U_0$ required to bring the loading device into contact with the loading rod was determined by a static loading experiment to be 0.6 V. This avoided impact collisions between the loading device and loading rod during the experiment. The maximum proportional valve voltage $U_{\text{max}}$ of the proportional valve was set to 3.5 V. The corresponding loading forces of the front and rear bearings were 150–450 N and 50–150 N, respectively. The effect of radial forces in the range of 0–30,000 rpm on the DSSB was tested at 6000 rpm intervals. After the HSMS ran stably at the experimental speed, it was loaded and the loading force and deformation displacement at four positions were measured simultaneously. The proportional valve voltage was gradually increased (0.1 V/s) from $U_0$ to $U_{\text{max}}$. The proportional valve voltage was maintained at $U_{\text{max}}$ for about 15 s and then gradually decreased (−0.1 V/s) to $U_0$. The above process was repeated 2–3 times to verify the repeatability of the experiment. The original experimental data of the HSMS at a speed of 24,000 rpm is shown in Figure 4. It shows that under the same loading force, the deformation displacement of the measuring points in the EMM was much larger than that in the IMM, which shows that the bending deformation displacement of the loading rod due to the cantilever beam cannot be ignored.

![Fig 4. Original experimental data of loading force and deformation displacement: $F_A$ and $F_B$ = loading forces of support points A and B in the equivalent model; $\delta_C$, $\delta_E$, $\delta_F$, and $\delta_G$ = deformation displacements of points C, E, F, and G, respectively, in the equivalent model ($n = 24,000$ rpm).](image-url)

Using the EMM and IMM described in Section 2.2 to analyse the experimental results, the relationship between the loading force and deformation displacement of the front/rear bearings at 24,000 rpm was derived (Figure 5). The original measured data (blue curves) was corrected by low-pass filtering (green curves); then, the one-to-one correspondence between loading force and deformation displacement (red curve) was obtained by
polynomial fitting. According to Figure 5, the radial deformation displacement \( \delta_r \) of the front/rear bearings increases with increases in the radial force \( F_r \). According to Equations (11) and (12), we can verify that the DSSB can be obtained by deducing the radial force \( F_r \) to the deformation displacement \( \delta_r \). That is, the polynomial model (red curve) is derived to obtain the DSSB.

![Graph showing the relationship between radial force and deformation displacement for different bearing configurations.](image)

**Fig 5** Radial force \( F_r \) vs deformation displacement \( \delta_r \) of the front/rear bearings measured by EMM and IMM (\( n = 24,000 \) rpm).

### 4.2 Effect of radial force on the DSSB

Figure 6 shows the experimental results regarding the effect of the radial force on the DSSB, including analyses by EMM and IMM. It can be seen from Figure 6 that, first, as the radial force \( F_r \) increases, the DSSB \( K_r \) increases nonlinearly. This is mainly because the radial force \( F_r \) makes the contact deformation of the half-turn rolling elements in the radial force direction increase, and the contact deformation of the other half-turn rolling elements decreases, but the overall resistance to deformation of the contact surface is increased\(^{17}\). Second, the trends of DSSB obtained by the EMM and IMM are consistent, but the EMM measurements are significantly less than those of IMM. This is mainly due to the tapered connection gap between the loading rod and the rotor, which makes the measured deformation displacement \( \delta_r \) of the loading rod larger in the EMM. Third, the stiffness of the front bearings (B7005/C) is greater than that of the rear bearings (B7003/C), which is mainly due to their larger size. Fourth, the experimental results of 2–3 loading and unloading cycles (as shown in Figure 4) show that both the
EMM and IMM have good repeatability. Although the EMM estimates the measured DSSB to be lower due to the tapered connection gap, it still has certain application value due to its convenient installation and lack of need to modify the structure and design of the HSMS. Moreover, the rotor operating stiffness measured by the EMM can better reflect the true anti-deformation ability of the HSMS. In contrast, the IMM can more accurately measure the DSSB by measuring the deformation displacement of the internal rotor, which provides a new way to experimentally verify the theoretical bearing stiffness models.

![Graph showing the effect of radial force on the radial stiffnesses of the front (left) and rear (right) HSMS bearings.](image)

**Fig 6 Effect of radial force on the radial stiffnesses of the front (left) and rear (right) HSMS bearings**

### 4.3 Effect of speed on the DSSB

The influence of speed on the DSSB is shown in Figure 7. The experimental results show that the experimental device and schemes proposed in this paper could effectively measure the DSSB at speeds of up to 30,000 rpm. It can be seen from Figure 7 that as the speed increases, the DSSB tend to decrease. This is mainly due to the fact that as the speed increases, the centrifugal force and gyroscopic moment push the rolling elements outward, resulting in a reduction in the contact area of the bearing rolling elements and inner ring, which reduces the bearing stiffness\(^{18}\). The rotor operating stiffness of the HSMS mainly depends on its DSSB and so will also decrease with increasing speed\(^{19}\).

![Graph showing the effect of speed on the radial stiffnesses of the front (left) and rear (right) HSMS bearings.](image)

**Fig 7 Effect of speed on the radial stiffnesses of the front (left) and rear (right) HSMS bearings**
4.4 Effect of working temperature on the DSSB

The temperature increases of the HSMS are more serious at high speed, so it is necessary to study the influence of working temperature on the DSSB. The working temperature of the HSMS was varied by controlling the flow of cooling water. During the experiments, the cooling water was pumped at maximum, half and zero speeds. The working temperatures of the front/rear bearings were measured by built-in temperature sensors (as shown in Figure 1). When the working temperatures of the bearings were basically stable, the EMM and IMM were used to measure the DSSB during a loading process. The average temperatures of the front/rear bearings during the loading process were taken as their working temperature. The influence of working temperature on the DSSB at an experimental HSMS speed of 24,000 rpm was obtained (Figure 8). Figure 8 shows that as the working temperature increases, the DSSB increase. This is mainly due to thermal expansion of the bearings due to the temperature rise, which made the contact between the rolling elements and the inner/outer rings closer and, ultimately, led to an increase in the DSSB. Although a higher operating temperature helps to increase the DSSB of the HSMS, it will seriously deteriorate the lubrication conditions and increase the contact load of the bearings, which will eventually lead to damage or wear of the HSMS. Therefore, it is very necessary to use circulating water to cool the HSMS rotor and bearings and the influence of temperature increases on the dynamic performance of HSMS cannot be ignored.

![Figure 8 Effect of working temperature on the radial stiffnesses of the front (left) and rear (right) HSMS bearings](image)

5. Conclusions

In this paper, a new method of dynamically loading a high-speed motorized spindle (HSMS) was proposed. Two experimental schemes for measuring the dynamic support stiffnesses of the front/rear bearings (DSSB) were studied. The influence of working-condition parameters on the DSSB was tested on the built test system. We obtained the following conclusions:

1) The experiments show that the dynamic loading device could load the HSMS smoothly at speeds as high as 30,000 rpm, which solves the loading problem in HSMS stiffness testing.

2) Because the tapered connection gap between the loading rod and rotor decreases the stiffness, the DSSB measured by the external measurement method (EMM)—where the DSSB is an indirect measurement made by
analysing the deformation displacements of two points on the external loading rod of the HSMS—was relatively small. However, because the EMM does not need to modify the structural design of the HSMS, it has high versatility and application value.

3) The internal measurement method (IMM)—where the DSSB is directly measured by eddy current sensors installed near the front/rear bearings—can more accurately measure the DSSB. This verifies the validity and correctness of the EMM and provides an experimental basis for the verification of theoretical bearing stiffness models.

4) The experimental results show that both the EMM and IMM have high repeatability. The DSSB decreases with speed and increases with radial force and working temperature.

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Declaration of conflicting interests
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Figures

**Figure 1**

Structure and equivalent model of the specially designed HSMS
Figure 2

Test system for rotor operating stiffness and DSSB of HSMS
Figure 3

Schematic diagram of HSMS radial loading

Figure 4

Original experimental data of loading force and deformation displacement: \( F_A \) and \( F_B \) = loading forces of support points A and B in the equivalent model; \( \delta_C, \delta_E, \delta_F, \) and \( \delta_G \) = deformation displacements of points C, E, F, and G, respectively, in the equivalent model (\( n = 24,000 \text{ rpm} \)).
Figure 5

Radial force $F_r$ vs deformation displacement $\delta_r$ of the front/rear bearings measured by EMM and IMM ($n = 24,000$ rpm).
Figure 6

Effect of radial force on the radial stiffnesses of the front (left) and rear (right) HSMS bearings

Figure 7

Effect of speed on the radial stiffnesses of the front (left) and rear (right) HSMS bearings
Figure 8

Effect of working temperature on the radial stiffnesses of the front (left) and rear (right) HSMS bearings.