Effective Majorana neutrino decay

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Abstract We study the decay of heavy sterile Majorana neutrinos according to the interactions obtained from an effective general theory. We describe the two- and three-body decays for a wide range of neutrino masses. The results obtained and presented in this work could be useful for the study of the production and detection of these particles in a variety of high energy physics experiments and astrophysical observations. We show in different figures the dominant branching ratios and the total decay width.

1 Introduction

The discovery of neutrino oscillations has been one of the most spectacular new results in high energy physics, and so far is the only compelling experimental evidence of the existence of physics beyond the Standard Model. The sub-eV left-handed neutrino masses required by neutrino oscillation data are very difficult to generate just by the addition of right-handed neutrinos to the Standard Model, as the Yukawa couplings should be very small compared to those of the other particles. The introduction of intermediate fermion heavy particles which are singlets under the SM gauge group—the right-handed Majorana neutrinos—allows for the generation of light neutrino masses by the seesaw mechanism [1–6].

For the conventional seesaw scenarios often studied, the light neutrino masses are inversely proportional to an unknown lepton number violating large scale $M_N$ such that $m_ν ≈ m_D^2/M_N$ where $m_D$ is a Dirac mass connected with the Yukawa coupling by $m_D = μν/√2$, being $ν$ the Higgs field vacuum expectation value. For Yukawa couplings of order $Y ≈ 1$ we need a Majorana mass scale of order $M_N ≈ 10^{15}$ GeV to account for a light $ν$ mass compatible with the current neutrino data ($m_ν ≈ 0.01$ eV). This scenario clearly leads to the decoupling of the heavy Majorana neutrino $N$. However, for smaller Yukawa couplings of the order $Y ≈ 10^{-8} − 10^{-6}$, sterile neutrinos with masses $M_N ≈ (1 − 1000)$ GeV could exist. Any way, in the simplest Type-I seesaw scenario with sterile neutrinos, this leads to a too small left-right neutrino mixing [7–9], $U_{iN}^2 ≈ m_ν/M_N ≈ 10^{-14} − 10^{-10}$. These values are several orders of magnitude smaller than the neutrinoless double beta decay (0νββ) or collider bounds, as will be shown later.

Thus, as it was explained in [9], the detection of Majorana neutrinos would be a signal of physics beyond the minimal seesaw mechanism leading to the well known $νSM$ lagrangian, and its interactions could be better described in a model-independent approach based on an effective theory, considering a scenario with only one Majorana neutrino $N$ and negligible mixing with the $ν_L$.

The possibilities of discovering heavy Majorana neutrinos have been and are still extensively investigated, for example involving production and decay in $e^+ e^−$ and $e^− P$ colliders [10–17], in $e^− γ$ and $γ γ$ colliders [18–20], in hadron colliders via lepton number violating dilepton signals [9,21–30], and recently including new production mechanisms [31–33]. Some searches are currently being performed in the LHC [34–37]. Also, we can mention recent inverse seesaw mechanism (ISS) [38–40] heavy neutrino production studies in collider contexts [41–44].

The study of sterile Majorana neutrino decays is an issue of great interest in different areas of high energy physics. Besides the mentioned detection in colliders by lepton number violation, other kinds of searches exploiting the displaced vertex and delayed photons techniques have been proposed and are taking place at the LHC [45–52]. Also, searches in neutrino telescopes like Ice Cube [53,54] have been proposed, and the new decay modes and their relation with the explanation of several anomalies as the sub-horizontal events detected by SHALON or the anomaly in MiniBoone [55,56] are being investigated [57,58]. In astrophysical envi-
ronments, the cosmic and the diffuse supernova neutrino backgrounds can be used to probe possible radiative decays and other decay modes of cosmological interest [59,60].

With these motivations in mind, in this work we study the decays of heavy Majorana neutrinos in a general, model-independent approach in the context of an effective theory. In Sect. 2 we present the effective operators and the analytical decay widths obtained for the different two-body and three-body channels. In Sect. 3 we present our numerical results for the found decay modes, and discuss the bounds imposed on the values for the effective couplings. Our final remarks are made in Sect. 4. The complete effective lagrangian and fermionic decay modes are left for the appendix.

2 Effective operators and decay widths

In this paper we consider the decays of a right-handed Majorana neutrino $N$. As it is a $SM$ singlet, the only possible renormalizable interactions with the $SM$ fields could occur via the Yukawa coupling, which as we mentioned earlier, must be very small if the $ν SM$ is to reproduce the observed tiny $ν L$ masses. In an alternative approach, in this paper we consider that the sterile $N$ interacts with the standard light neutrinos by effective operators of higher dimension. We consider this effective interaction to be dominant compared to the mixing via the Yukawa couplings, so we depart from the traditional viewpoint in which the sterile neutrinos mixing with the standard neutrinos is assumed to govern the production and decay mechanisms for the $N$.

In this approach we parameterize the effects of new physics beyond the standard model by a set of effective operators $O$ constructed with the standard model and the Majorana neutrino fields and satisfying the Standard Model $SU(2)_L \otimes U(1)_Y$ gauge symmetry [61]. The effect of these operators is suppressed by inverse powers of the new physics scale $Λ$ which is not necessarily related to the mass $m_N$ for which we take the value $Λ = 1$ TeV [62].

The total lagrangian is organized as follows:

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{n=6}^{\infty} \frac{1}{Λ^{n-4}} \sum_i α_i O_i^{(n)}. \tag{1}$$

For the considered operators we follow [9] starting with a rather general effective lagrangian density for the interaction of right-handed Majorana neutrinos $N$ with leptons and quarks. All the operators we list here are of dimension 6 and could be generated at tree-level in the unknown fundamental high energy theory. The first subset includes operators with scalar and vector bosons (SVB),

$$O_{LNφ} = (\bar{φ}^T i \gamma μLφ)(\bar{N}i γ μN), \quad O_{NNφ} = i (φ^T D_μφ)(\bar{N}γ μN), \quad O_{Neφ} = i (φ^T D_μφ)(\bar{N}γ μe_i) \tag{2}$$

and a second subset includes the baryon-number conserving four-fermion contact terms:

$$O_{dNNe} = (\bar{d}_i γ μu_i)(\bar{N}γ μe_i), \quad O_{fNN} = (\bar{f}_j γ μf_j)(\bar{N}γ μN), \quad O_{LNLε} = (\bar{L}_1 Nε)(\bar{L}_1 ε), \quad O_{LNQd} = (\bar{L}_1 Nε)(\bar{Q}_d d_i),$$

$$O_{QuNL} = (\bar{Q}_i u_i)(\bar{N}L_i), \quad O_{QNLe} = (\bar{Q}_i Nε)(\bar{L}_i d_i), \quad O_{LN} = |\bar{N}L_i|^2. \tag{3}$$

where $e_i, u_i, d_i$ and $L_i, Q_i$ denote, for the family labeled $i$, the right-handed $SU(2)$ singlet and the left-handed $SU(2)$ doublets, respectively.

In addition, there are operators generated at one-loop level in the underlying full theory whose coefficients are naturally suppressed by a factor $1/16π^2 [9,63]:$

$$O_{NNB}^{(5)} = \bar{N}σ_{μν}N^c B_{μν}, \quad O_{NB} = (Lσ_{μν}N)φB_{μν}, \quad O_{NW} = (Lσ_{μν}τ^1 N)φW_{μν},$$

$$O_{DN} = (\bar{L}D_μN)D^μφ, \quad O_{DN} = (D_μ\bar{L}N)D^μφ. \tag{4}$$

2.1 Two-body decays

The two-body decay channels for the heavy Majorana neutrino $N$ are shown in Fig. 1. They receive contributions from the lagrangian terms originating with operators involving gauge bosons and the Higgs field, presented in (2) and (4), that lead to the effective lagrangian presented in (A1) and (A3).

The analytical expressions obtained for the decay widths of channels $N → νZ, N → l^+ l^- N, N → νh$ shown in Fig. 1 are

$$\Gamma^{N → νZ} = \left(\frac{m_N}{128π}\right)^4 \left(\frac{m_N}{Λ}\right)^4 (1−yz)^2 \left[α_{L4}^{(i)}α_{L4}^{(i)}(1−yz)^2 + 8α_{L4}^{(i)}α_{L4}^{(i)}α_{sW}^{(i)}cW − α_{L4}^{(i)}sW\right](1−yz)y_v$$

$$+ 16(2 + yz)y_v(α_{L4}^{(i)}cW − α_{L4}^{(i)}sW)^2\right]$$

with $y_Z = m_Z^2/m_N^2$ and $y_v = v^2/m_N^2$;

$$\Gamma^{N → l^+ l^- N} = \left(\frac{m_N}{32π}\right)^4 \left(\frac{m_N}{Λ}\right)^4 2α_{W}^{(i)}(1−yw)^2(1+2yw)y_v$$

with $y_W = m_W^2/m_N^2$;

$$\Gamma^{N → νh} = \left(\frac{9m_N}{128π}\right)^4 \frac{v^4}{Λ^4} α_{φ}^{(i)}(1−yh)$$

with $y_h = m_h^2/m_N^2$.

Finally, we have the decay mode to a photon and an ordinary neutrino, $N → νA$:

$$\Gamma^{N → νA} = \left(\frac{v^2}{m_N}\right)^4 \left(\frac{m_N}{Λ}\right)^4 (α_{L4}^{(i)}cW + α_{L4}^{(i)}sW)^2. \tag{5}$$

This decay mode leads to an interesting phenomenology, part of which was discussed in [58].
The three-body decays of the heavy Majorana neutrino $N$ involving gauge bosons and the Higgs field receive contributions from the lagrangians presented in (A1) and (A3), whereas the decays to three fermions come also from the operators presented in (3). The effective model we are working with also gives tree-level contributions to four-body decays, but as their contributions are very small, they are not presented in this work.

The three-body decay channels involving gauge bosons and ordinary neutrinos are shown in Fig. 2; (a) and (b) $N \rightarrow \nu W^+ W^-$, (c) and (d) $N \rightarrow \nu ZZ$, and (e) $N \rightarrow \nu Z A$.

The analytical expressions for the decay widths are

\[
\frac{d\Gamma^{N \rightarrow \nu W^+ W^-}}{dx} = \frac{m_N}{64\pi^3} \left( \frac{m_N}{\Lambda} \right)^4 \frac{\alpha^{\text{emg}}}{x^2} \frac{2}{(1-x)^2 y_W} \times \left( (1-x)(1-x-4y_W) \right)^{1/2} \times \left[ 16\alpha^{(i)}_{L_3}(3-x)((1-x)^2 \right. \\
+ 4(1-x)y_W - 8y_W^2) \\
+ 3 |\tilde{\alpha}^{(i)}|^2 \frac{1}{(1-x)(1-x)^2} \\
- 4(1-x)y_W + 12y_W^2 \left. \right] 
\]

where $\tilde{\alpha}^{(i)} = \alpha^{(i)}_{L_3} + \frac{3}{2} y_{W_L} \left( 1 - \frac{y_W}{\sqrt{y_W+1}} \right)$, $y_{W_L} = \frac{\Gamma_W}{m_N^2}$. In this process we discard the $N \rightarrow lW$ followed by the $l \rightarrow \nu W$ SM vertex contribution, because the amplitude is proportional to the intermediate lepton mass, and thus negligible in comparison with the diagrams shown in Fig. 2(a), (b).

\[
\frac{d\Gamma^{N \rightarrow \nu ZZ}}{dx} = \frac{m_N}{64\pi^3} \left( \frac{m_N}{\Lambda} \right)^4 \frac{\alpha^{\text{emg}}}{x^2} \frac{2}{y_Z} \times \left[ \left( \frac{y^{(i)}_{L_i}}{1-x-y_h} \right)^2 + \frac{3}{y_{W_L}} \left( \frac{y^{(i)}_{L_i}}{1-x-y_h} \right)^2 \frac{2}{y_h y_{\Gamma_h}} \right] \\
\times \frac{x^2}{(1-x)} \left[ 2 + (1-x-2y_Z)^2 \right] \times (1-x) \times 4y_Z^2 \times (1-x-2y_Z)^{1/2} 
\]

with $\alpha^{\text{emg}}$ being the electromagnetic constant, and $y_{\Gamma_h} = \Gamma_h^2/m_N^2$.

\[
\frac{d\Gamma^{N \rightarrow \nu Z A}}{dx} = \frac{m_N}{32\pi^3} \left( \frac{m_N}{\Lambda} \right)^4 \frac{\alpha^{\text{emg}}}{x^2} \times \left( c_W \alpha^{(i)}_{L_i} + s_W\alpha^{(i)}_{L_3} \right)^2 \times \frac{2}{(1-x)^3} (1-x^2 y_Z)^3 
\]

The three-body channels with Higgs fields in the final state are shown in Fig. 3 (a) $N \rightarrow \nu hh$, (b) $N \rightarrow l^+W^-h$, (c) $N \rightarrow \nu h A$, and (d) $N \rightarrow \nu h Z$. The obtained expressions for the decay widths are
Three-body decays with gauge bosons and Higgs field

\[
\frac{d\Gamma^{N\rightarrow l^+W^-}}{dx} = \frac{m_N g^2}{214\pi^3} \frac{m_N}{\Lambda} \frac{\mu}{m_N}^2 \left( 1 - \frac{x}{y_h} \right) \left( y_W - 4y_W^2 \right)^{1/2} (1 - x),
\]

with \(0 \leq x \leq 1 - y_h\);

\[
\frac{d\Gamma^{N\rightarrow l^+W^-}}{dx} = \frac{9 m_N g^2}{214\pi^3} \frac{m_N}{\Lambda} \frac{\mu}{m_N}^2 \left( \left( 1 - \frac{x}{y_h} \right)^2 - 4y_W^2 \right)^{1/2} \left( 1 - x + y_h \right)
\]

with \(2\sqrt{y_h} \leq x \leq 1 + y_h - y_z\). This decay width is obtained from the diagram shown in Fig. 3(d), as this contribution involves a tree-level vertex coming from the lagrangian (A1) and a SM vertex, and is dominant comparing to the one-loop level term coming from the lagrangian (A3), that would give a vertex as the one shown in Fig. 3(c).

The three-body decay channel with two gauge bosons and charged leptons in the final state are shown in Fig. 4, where \(N \rightarrow l^+W^-A, Z\). We cannot obtain analytical expressions for these decay widths, and we have done numerical integrations of the phase space in the usual way using the numerical routine RAMBO [64].

Some of the three-body decays involving only fermions in the final state come from the four-fermion contact operators presented in (3). These operators lead to the tree-level lagrangian in (A2).

The partial decay widths of a heavy Majorana neutrino \(N\) decaying to three fermions were calculated including the contributions in the effective lagrangians (A1) and (A2). The decay channels are shown in Fig. 5. As was previously mentioned, the diagrams (a) and (b) show the resonant contributions coming from two-body decays to \(W\) and \(h\) bosons. The analytical expressions obtained were presented in our previous work [58], and for completeness we display them in Appendix B.
3 Numerical branching ratios and total decay width

The numerical results for the Majorana neutrino branching ratios and total decay width are presented in the following. In Figs. 6 and 7 we show the results for the branching ratios for the different decay channels found in the previous section. We display the branching ratios as a function of the Majorana neutrino mass $m_N$, calculated for different numerical values of the constants $\alpha_i$. In all the following results, when ordinary neutrinos are present in the final states, we sum the contributions of the neutrino and antineutrino channels. It is important to realize that, as we explained in the introduction, we are neglecting the contributions of the $N-\nu_L$ mixings compared to the effective interactions. In this condition the effective contribution to the branching ratios that we present here are dominant for the scale $\Lambda = 1$ TeV considered and for the values of $\alpha$ allowed by experimental data, as will be explained in the next section.

![Fig. 6](image1.png)  
(a) Three fermion and neutrino-photon decay channels.

![Fig. 7](image2.png)  
(b) Massive gauge and Higgs boson decay channels

Fig. 6 The Branching ratios for the Majorana neutrino decay in the set A considering the sum of families

The values for the coupling constants $\alpha$ are limited by bounds coming from electroweak precision data (EWPD) and $0\nu\beta\beta$-decay data. In order to simplify the discussion we consider just two numerical sets of values: in set A the couplings associated to the operators that contribute to the $0\nu\beta\beta$-decay are restricted to the corresponding bound, $\alpha_{0\nu\beta\beta}^{\text{bound}}$ (8) and the other constants are restricted to the bound determined by EWPD $\alpha_{\text{EWPD}}^{\text{bound}}$ (9) (see next section). In the case of the set B all the couplings are restricted to the $0\nu\beta\beta$ bound $\alpha_{0\nu\beta\beta}^{\text{bound}}$, which is the most stringent. The branching ratios, being quotients between partial widths, take very similar numerical values for the two sets.

In Fig. 6a we present the branching ratios of the three-fermion and photon–neutrino channels for the couplings set A. These are the only open channels for Majorana neutrino masses below $m_W$. As it can be seen, for low $m_N$ the dominant mode is the decay of $N$ to a photon and a neutrino. Taking the values of the couplings $\alpha^{(i)}$ to be equal for every family $i$, and also for every tree-level coupling $\alpha^{\text{tree}}$, and taking the one-loop generated couplings as $\alpha^{1\text{-loop}} = \alpha^{\text{tree}}/16\pi^2$, we derived an approximated expression for the ratio between the widths $\Gamma(N \rightarrow \nu(\bar{\nu})A)$ in (5) and $\Gamma(N \rightarrow l^+\bar{u}d)$ in (B1):

$$\frac{\Gamma(N \rightarrow \nu(\bar{\nu})A)}{\Gamma(N \rightarrow l^+\bar{u}d)} \rightarrow \frac{2}{15\pi} \left(\frac{\nu}{m_N}\right)^2 \left(c_W + s_W\right)^2.$$

This limiting value explains the behavior found in Fig. 6a, showing the neutrino plus photon decay channel is clearly dominating for low $m_N$ (in [58] we verify that this channel still dominates over the decay of $N$ to QCD-mesons like pions). This is an interesting fact since we have a new source of photons in astrophysical environments. The implications of this new channel for the MiniBoone [65] and SHALON [66] anomalies were discussed in our previous work [58].
and turn them into constraints on the effective couplings
the existing bounds for the sterile-active neutrino mixings (LNV) meson decays and direct collider searches, including
low energy observables as rare lepton number violating

Figure 6(b) shows the massive gauge and Higgs boson decay channels for the \( N \). The branching ratio for the \( N \to \nu hA \) mode is smaller than \( 1 \times 10^{-7} \) and is not visible in the plot.

For completeness we present the branching ratios for the
two-body decay channels. As we explained in the previous
section, the \( N \to \nu h, W \) channels are not included in the
total width, as their contribution has already been taken into
account in the channels where the \( W \) and \( h \) bosons participate
as intermediate resonant states.

Finally, Fig. 8 shows the total decay width dependence on
the mass \( m_N \) for both coupling sets considered, and again a
sum over families and channels with particles and antiparti-
cles in the final state is performed.

3.1 Bounds on the couplings \( \alpha^i_{\mathcal{O}} \)

The effective couplings \( \alpha^i_{\mathcal{O}} \) can be bounded exploiting the
existing constraints coming from neutrinoless double beta
decay (0\( \nu \)\( \beta \beta \)), electroweak precision data tests (EWPD),
low energy observables as rare lepton number violating
(LNV) meson decays and direct collider searches, including
\( Z \) decays. We explain here in detail how we take account of
the existing bounds for the sterile-active neutrino mixings and
turn them into constraints on the effective couplings \( \alpha^i_{\mathcal{O}} \).
In the literature, the bounds are generally imposed on the
parameters representing the mixing between the ster-
ile and active left-handed ordinary neutrinos. Very recent
reviews [7,8,16,67] summarize in general phenomenological
approaches the existing experimental bounds, consid-
ering low scale minimal seesaw models, parameterized by a
single heavy neutrino mass scale \( M_N \) and a light–heavy mixing \( U_{iN} \), with \( l \) indicating the lepton flavor. In the effective
lagrangian framework we are studying, the heavy Majorana
neutrino couples to the three fermion family flavors with cou-
plings dependent on the new ultraviolet physics scale \( \Lambda \) and
the constants \( \alpha^i_{\mathcal{O}} \). We can interpret the current bounds comparing our couplings with the general structure usually taken
for the interaction between heavy neutrinos with the standard
gauge bosons [68,69]:

\[
\mathcal{L}_W = -\frac{g}{\sqrt{2}} \gamma^\mu U_{1N} P_L N W_\mu + h.c.
\]

\[
\mathcal{L}_Z = -\frac{g}{2c_W} \bar{\nu}_{L\mu}^\mu U_{1N} P_L N Z_\mu + h.c.
\]

(6)

The operators presented in (2) lead to a term in the effective
lagrangian (A1) that can be compared to the interaction in (6)
for the weak charged current, giving a relation between the
coupling \( \alpha^i_{W} \) and the mixing \( U_{1iN} \): \( U_{1iN} \simeq \frac{\alpha^i_{W} v^2}{2\Lambda^2} \) [9]. Never-
thless, as we are neglecting the \( N-\nu_L \) neutrino mixing, no
operators lead to a term that can be directly related—with the
same Lorentz–Dirac structure—to the interaction in (6)
for the neutral current (nor at tree or one-loop level). Some
terms in the lagrangian (A3) contribute to the \( ZN\nu \) coupling,
but as they are generated at one-loop level in the ultraviolet
underlying theory, they are suppressed by a \( 1/16\pi^2 \) factor. In
consequence, we take a conservative approach and in order to
keep the analysis as simple as possible—but with the aim to
put reliable bounds on our effective couplings—in this work
we relate the mixing angle between light and heavy neutrinos
\( (U_{eN}, U_{\mu N}, U_{\tau N}) \) with the couplings as \( U \simeq \frac{\alpha^i_{O} v^2}{2\Lambda^2} \), where \( v \)
corresponds to the vacuum expectation value: \( v = 250 \text{ GeV} \).

As has been remarked in [7,8], the bounds for low ster-
ile neutrino masses, coming from beam dump and rare LNV
decays of mesons, are heavily dependent on the decay modes
considered. As the effective lagrangian we are considering
leads to the decay mode to a photon and an ordinary neu-
trino, those bounds do not apply in this work. For \( m_N \) in
the range above a few hundred GeV, the electroweak pre-
cision data involving lepton number violating processes put
the most stringent bounds on the neutrino mixings, except
for the coupling constants of the first fermions family where
the most stringent limits come from 0\( \nu \beta \beta \)-decay. For the
second and third families, we find that the most restric-
tive are the EWPD constraints. In the following we explain
how these bounds are translated to the effective couplings \( \alpha^i_{O} \).

Some of the considered operators contribute directly to the
neutrinoless double beta decay (0\( \nu \beta \beta \)-decay) and thus the

In a general way, the following effective interaction
Hamiltonian can be considered:

\[
\mathcal{H} = G_{\text{eff}} \bar{u} \Gamma \bar{d} \bar{e} \Gamma N + h.c.
\]

(7)
where $\Gamma$ represents a general Lorentz–Dirac structure. Following the development presented in [70] we find

$$G_{\text{eff}} \leq A \times 10^{-8} \left( \frac{m_N}{100 \text{ GeV}} \right)^{1/2} \text{ GeV}^{-2}$$

where the numerical constant $A$ depends on the nuclear model used and the lifetime for the $0\nu\beta\beta$-decay. We take the most stringent limit $\tau_{0\nu\beta\beta} \geq 1 \times 10^{26}$ years obtained by the KamLAND-Zen Collaboration [71].

In the effective theory we are considering the lowest order contribution to $0\nu\beta\beta$-decay comes from the operators containing the $W$ field and the four-fermion operators with quarks $u,d$, the lepton $e$, and the Majorana neutrino $N$. These operators contribute to the effective Hamiltonian (7), with $G_{\text{eff}} = \frac{\alpha}{\Lambda^2}$, which, as we discussed in the paragraph after Eq. (6), is related with the mixing angle between light and heavy neutrinos as $U_{\mu N}^2 = \left( \frac{\alpha}{2 \Lambda^2} \right)^2$. We find that the value $A = 3.2$ fits very well the bounds obtained for the mixings [72,72] in the literature.

We can translate the limit coming from $G_{\text{eff}}$ on $\alpha_O^{(1)}$, which, for $\Lambda = 1 \text{ TeV}$, is

$$\alpha_{0\nu\beta\beta}^{\text{bound}} \leq 3.2 \times 10^{-2} \left( \frac{m_N}{100 \text{ GeV}} \right)^{1/2}. \quad (8)$$

On the other hand, to consider the existing bounds coming from collider, electroweak precision data (EWPD) and lepton-flavor-violating (LFV) processes we define, following [73]: $\Omega_{ll'} = U_{lN} U_{l'N}$ where the allowed values for the parameters are [74]:

$$\Omega_{ee} \leq 0.0054, \quad \Omega_{\mu\mu} \leq 0.0096, \quad \Omega_{\tau\tau} \leq 0.016.$$

For the LFV process, e.g. $\mu \rightarrow e\gamma$, $\mu \rightarrow eee$ and $\tau \rightarrow eee$, which are induced by the quantum effects of the heavy neutrinos, we have several bounds [27,67,75,76] but the most restrictive one comes from $Br(\mu \rightarrow e\gamma) \leq 5.7 \times 10^{-13}$ [76,77]. This bound imposes $|\Omega_{e\mu}| \leq 0.0001$, and can be translated to the constants $\alpha$,

$$\Omega_{e\mu} = U_{eN} U_{\mu N} = \left( \frac{\alpha v^2}{2 \Lambda^2} \right)^2 < 0.0001,$$

and for $\Lambda = 1 \text{ TeV}$ we have

$$\alpha_{\text{EWPD}}^{\text{bound}} \leq 0.32. \quad (9)$$

In order to simplify the discussion, for the numerical evaluation we only consider the two following situations. In the set we call $A$ the couplings associated to the operators that contribute to the $0\nu\beta\beta$-decay ($O_{Ne\phi}$, $O_{duNe}$, $O_{QuNL}$, $O_{LNQd}$, and $O_{QNld}$) for the first family are restricted to the corresponding bound $\alpha_{0\nu\beta\beta}^{\text{bound}}$ and the other constants are restricted to the bound determined by EWPD $\alpha_{\text{EWPD}}^{\text{bound}}$. In the case of the set called $B$ all the couplings are restricted to the $0\nu\beta\beta$ bound $\alpha_{0\nu\beta\beta}^{\text{bound}}$, which is the most stringent. For the 1-loop generated operators we consider the coupling constant as $1/(16\pi^2)$ times the corresponding tree-level coupling: $\alpha_1^{\text{loop}} = \alpha_{\text{tree}}/(16\pi^2)$. Thus, for the operators $O_{DN}$, $O_{NW}$ and $O_{DN}$, which contribute to $0\nu\beta\beta$, we have

$$\alpha_{L_2}^{(1)}, \alpha_{L_3}^{(1)}, \alpha_{L_4}^{(1)} \sim \frac{1}{16\pi^2} \alpha_{0\nu\beta\beta}^{\text{bound}}$$

for fermions of the first family. For the remaining operators we take

$$\alpha \sim \alpha_{\text{EWPD}}, \alpha_{0\nu\beta\beta}^{\text{bound}}$$

in the sets $A$ and $B$, respectively.

4 Final remarks

Searches for heavy neutrinos often rely on the possibility that they may decay to detectable particles. The interpretation of the corresponding results of such searches requires a model for the heavy neutrino decay. In this work we consider an effective approach for heavy Majorana neutrino interactions, and we calculate the branching ratios for the different decay modes.

Depending on the Majorana neutrinos mass scale, the decay can have effects on different physical contexts like solar/astrophysical neutrinos, collider searches like the ones taking place at the LHC, neutrino experiments as OPERA, MiniBoone, SHALON, etc. In particular, the effects of some of these experiments for low mass neutrinos were discussed in [58].

Summarizing, we calculated the decay modes for the Majorana neutrinos $N$ in an effective theory approach. We presented the analytical results for the dominant channels, discussed the existent bounds taken into account for the effective couplings, and displayed the different branching ratios and the total decay width for the heavy sterile neutrino considered.

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Appendix A: Complete effective lagrangian

We present here the complete effective lagrangian obtained from the operators listed in (2), (3) and (4). The full contributions are considered for the total Majorana neutrino decay width $\Gamma_N$,

$$L_{\text{eff}}^{\text{tree}} = \frac{1}{\Lambda^2} \left\{ \alpha_\phi^{(i)} \left( \frac{3v^2}{2\sqrt{2}} \bar{\nu}_l,i N_R h + \frac{3v}{2\sqrt{2}} v_\mu N_R h h \right) + \frac{1}{2\sqrt{2}} \bar{\nu}_l,i N_R h h h \right\} - \alpha_Z \left( -\bar{\nu}_R \gamma^\mu N_R \left( \frac{m_Z}{v} Z_\mu \right) \left( \frac{v^2}{2} + v h + \frac{1}{2} h h \right) \right) + \bar{\nu}_R \gamma^\mu N_R \left( \frac{v}{2} P_\mu^{(h)} h + \frac{1}{2} P_\mu^{(h)} h h \right) - \alpha_W \left( \bar{\nu}_R \gamma^\mu l_R \left( \frac{v m_W}{\sqrt{2}} W^+ \mu + \sqrt{2} m_W W^+_\mu h \right) + \frac{g}{2\sqrt{2}} W^+ h h \right) + h.c. \right\}. \quad (A1)$$

In (A1) a sum over the family index $i$ is understood, and the constants $\alpha^{(i)}_O$ are associated to the specific operators:

$$\alpha_Z = \alpha_{N N \phi}, \quad \alpha_\phi^{(i)} = \alpha_{L N \phi}^{(i)}, \quad \alpha_W = \alpha_{N e \phi}^{(i)}.$$ 

The four-fermion contact operators presented in (3) lead to the tree-level lagrangian:

$$L_{\text{tree}}^{4-f} = \frac{1}{\Lambda^2} \left\{ \alpha_{V_0}^{(i)} \bar{\nu}_l,i \gamma^\mu u_R,i \bar{\nu}_R \gamma^\mu l_R,i \bar{\nu}_R \gamma^\mu N_R + \alpha_{V_1}^{(i)} \bar{\nu}_l,i \gamma^\mu l_R,i \bar{\nu}_R \gamma^\mu N_R + \alpha_{V_2}^{(i)} \bar{\nu}_l,i \gamma^\mu u_R,i \bar{\nu}_R \gamma^\mu N_R \right\} + \alpha_L^{(i)} \bar{\nu}_l,i \gamma^\mu l_R,i \bar{\nu}_R \gamma^\mu N_R + \alpha_G^{(i)} \bar{\nu}_l,i \gamma^\mu u_R,i \bar{\nu}_R \gamma^\mu N_R + \alpha_S^{(i)} \left( \bar{\nu}_l,i N_R e_l,i N_R + \bar{\nu}_R e_l,i e_l,i N_R \right) + h.c. \right\}. \quad (A2)$$

In (A2) a sum over the family index $i$ is understood, and the constants $\alpha^{(i)}_O$ are associated to the specific operators:

$$\alpha_{V_0}^{(i)} = \alpha_{d NN e}^{(i)}, \quad \alpha_{V_1}^{(i)} = \alpha_{e NN e}^{(i)}, \quad \alpha_{V_2}^{(i)} = \alpha_{L NN e}^{(i)}, \quad \alpha_L^{(i)} = \alpha_{d NN e}^{(i)}, \quad \alpha_S^{(i)} = \alpha_{L NN e}^{(i)}. \quad \alpha_{V_0}^{(i)} = \alpha_{d NN e}^{(i)}, \quad \alpha_{V_1}^{(i)} = \alpha_{e NN e}^{(i)}, \quad \alpha_{V_2}^{(i)} = \alpha_{L NN e}^{(i)}, \quad \alpha_L^{(i)} = \alpha_{d NN e}^{(i)}, \quad \alpha_S^{(i)} = \alpha_{L NN e}^{(i)}.$$ 

The one-loop level generated operators in (4) give the lagrangian:

$$L_{\text{eff}}^{1\text{-loop}} = \frac{\alpha_{L_1}^{(i)}}{\Lambda^2} \left\{ -i\sqrt{2} u c W P_{\mu}^{(A)} \bar{\nu}_l,i \sigma^{\mu \nu} N_R A_\nu^l + i\sqrt{2} u s W P_{\mu}^{(Z)} \bar{\nu}_l,i \sigma^{\mu \nu} N_R Z_\nu^l \right\} + i\sqrt{2} c W P_{\mu}^{(A)} \bar{\nu}_l,i \sigma^{\mu \nu} N_R A_\nu^l + i\sqrt{2} s W P_{\mu}^{(Z)} \bar{\nu}_l,i \sigma^{\mu \nu} N_R Z_\nu^l \right\} + m_W p_{\mu}^{(N)} \bar{\nu}_l,i N_R W^{-\mu} + \sqrt{2} m_W p_{\mu}^{(N)} \bar{\nu}_l,i N_R W^{-\mu} h + \frac{1}{\sqrt{2}} p_{\mu}^{(h)} p_{\mu}^{(N)} \bar{\nu}_l,i N_R h \right\} + i\sqrt{2} u s W P_{\mu}^{(A)} \bar{\nu}_l,i \sigma^{\mu \nu} N_R A_\nu^l + i\sqrt{2} c W P_{\mu}^{(Z)} \bar{\nu}_l,i \sigma^{\mu \nu} N_R Z_\nu^l \right\} + i2 m_W E_{\mu}^{(N)} W^{-\mu} + i2 m_W E_{\mu}^{(A)} W^{-\mu} h + i2 g c W l_{\mu}^{(N)} W^{-\mu} h + i2 g s W l_{\mu}^{(A)} W^{-\mu} h + i\sqrt{2} c W P_{\mu}^{(A)} \bar{\nu}_l,i \sigma^{\mu \nu} N_R A_\nu^l + i\sqrt{2} c W P_{\mu}^{(A)} \bar{\nu}_l,i \sigma^{\mu \nu} N_R A_\nu^l + i\sqrt{2} g s W Z_{\mu} + h.c. \right\}. \quad (A3)$$
where $P_1^{(d)}$ is the 4-moment of the incoming $a$-particle and a sum over the family index $i$ is understood again. The constants $\alpha_{L_1}^{(i)}$ with $j = 1, 2, 3, 4$ are associated to the specific operators:

$$
\alpha_{L_1}^{(i)} = \alpha_{N_1}^{(i)}, \quad \alpha_{L_2}^{(i)} = \alpha_{D_1}^{(i)}, \quad \alpha_{L_3}^{(i)} = \alpha_{N_2}^{(i)}, \quad \alpha_{L_4}^{(i)} = \alpha_{D_2}^{(i)}.
$$

Appendix B: Fermionic three-body decay widths

For the decays to one lepton and two quarks we have the expressions

$$
d\Gamma^{(N\rightarrow l\bar{u}d)}_N = \frac{m_N}{512\pi^3} \left( \frac{m_N^4}{\Lambda} \right)^4 \frac{\alpha_{L_1}^{(i)}}{(1-x+y_1+y_2)\sqrt{y_1y_2}}
$$

with $2\sqrt{y_1} < x < 1+y_1+y_2$, $y_1 = m_1^2/m_N^2$, $y_2 = m_2^2/m_N^2$, and for the terms $\alpha_{1,2,3,4}$

$$
\begin{align*}
\alpha_{j_1-j_1}^{(i)} &= (\alpha_{s_1}^{(i)2} + \alpha_{s_2}^{(i)2} - \alpha_{s_3}^{(i)2} - \alpha_{s_4}^{(i)2}) \delta_{j_1-j_1}, \\
\alpha_{j_2-j_1}^{(i)} &= \left( \alpha_{s_1}^{(i)2} \alpha_{s_1}^{(i)} - \alpha_{s_2}^{(i)2} \right) \delta_{j_2-j_1}, \\
\alpha_{j_3-j_1}^{(i)} &= \left( \alpha_{s_3}^{(i)2} + 4\alpha_{s_3}^{(i)2} \right) \delta_{j_3-j_1}, \\
\alpha_{j_4-j_1}^{(i)} &= \delta_{s_4}^{(i)2} \delta_{j_4-j_1}.
\end{align*}
$$

$$
\begin{align*}
d\Gamma^{(N\rightarrow l\bar{l}d)}_N = \frac{m_N}{128\pi^3} \left( \frac{m_N^4}{\Lambda} \right)^4 \frac{\alpha_{L_1}^{(i)} + \alpha_{L_2}^{(i)} + \alpha_{L_3}^{(i)} + \alpha_{L_4}^{(i)} + \alpha_{d}^{(i)} - \alpha_{s}^{(i)} - \alpha_{a}^{(i)} - \alpha_{e}^{(i)}}{(1-x+y_1+y_2)\sqrt{y_1y_2}}
\end{align*}
$$

with $0 < x < 1-4y_1+y_2$, $y_1 = m_1^2/m_N^2$, and

$$
\begin{align*}
\alpha_{j_1-j_1}^{(i)2} &= \frac{\alpha_{s}^{(i)}(1-x+y_1+y_2)}{D_h}, \\
\alpha_{j_2-j_1}^{(i)2} &= \frac{\alpha_{s}^{(i)}(1-x+y_1+y_2)}{D_h} , \\
\alpha_{j_3-j_1}^{(i)2} &= \frac{\alpha_{s}^{(i)}(1-x+y_1+y_2)}{D_h} , \\
\alpha_{j_4-j_1}^{(i)2} &= \frac{\alpha_{d}^{(i)}(1-x+y_1+y_2)}{D_h} .
\end{align*}
$$

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