Single Proton Knock-Out Reactions from $^{24,25,26}$F

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The cross sections of the single proton knock-out reactions from $^{24}$F, $^{25}$F, and $^{26}$F on a $^{12}$C target were measured at energies of about 50 MeV/nucleon. Ground state populations of 6.6±0.9 mb, 3.8±0.6 mb for the reactions $^{12}$C($^{24}$F,$^{23}$O) and $^{12}$C($^{25}$F,$^{24}$O) were extracted, respectively. The data were compared to calculations based on the many-body shell model and the eikonal theory. In the reaction $^{12}$C($^{26}$F,$^{25}$O) the particle instability of $^{25}$O was confirmed.

I. INTRODUCTION

The structure of neutron-rich nuclei in the $p/sd$-shell region has attracted significant interest recently [1]. The disappearance of the $N=20$ shell sparked the interest especially in the oxygen and fluorine isotopes [2,3,4]. Interaction-, reaction-, and charge-changing cross section (factors [11,12,13]. The single proton stripping reactions are a useful tool to extract spectroscopic information as well as fragmentation cross sections [6] have been measured and analyzed. However, a more detailed knowledge of properties of nuclei in this region is essential to understand the nuclear structure along the dripline.

In view of the emergence of the $N=16$ shell it has been suggested that the normal level structure is already influenced in $^{23}$O [5]. One would expect that the ground state of $^{23}$O is an $s_{1/2}$ level with strong single particle character. However, in order to explain the measured momentum distribution it was necessary to modify the core ($^{20}$O) structure [5]. This interpretation is controversial because an analysis of the data based on the many-body shell model and eikonal theory did not confirm the need for any changes of the level structure in $^{23}$O [6,10].

Recently, it has been shown that one-nucleon knock-out reactions are a useful tool to extract spectroscopic factors [11,12,13]. The single proton stripping reactions ($^{24}$F,$^{23}$O) and ($^{25}$F,$^{24}$O) should be sensitive reactions to study the ground state properties of $^{23}$O and $^{24}$O. Although experimentally not confirmed the ground state of $^{24}$F is most likely a $3^+$ state composed of $\pi d_{5/2}$ coupled to a $\nu s_{1/2}$ [14] and the ground-state of $^{25}$F is supposed to be the $\pi d_{5/2}$ state. Thus the reactions ($^{24}$F,$^{23}$O) and ($^{25}$F,$^{24}$O) should have strong couplings to the ground state of $^{23}$O and $^{24}$O, respectively.

We have measured single-proton knocked-out cross section of $^{24}$F, $^{25}$F, and $^{26}$F to populate states of $^{22}$O, $^{23}$O, and $^{24}$O. In most cases it is necessary to measure the reaction in coincidence with $\gamma$-rays to cleanly identify the populated state [12,15,16]. However, the search for excited states in the last bound oxygen isotopes $^{23}$O and $^{24}$O have been negative [7] so $\gamma$-ray coincidence measurements are not necessary in the present cases to identify the final state. The knock-out reaction of the heaviest fluorine isotope feasible up-to-date ($^{26}$F,$^{25}$O) leads to the particle-unstable nucleus $^{25}$O [17].

II. EXPERIMENTAL SETUP

The experiments were performed at the Coupled Cyclotron Facility of the National Superconducting Cyclotron Laboratory at Michigan State University [18,19,20]. A 110 MeV/nucleon $^{48}\text{Ca}^{19+}$ beam was fragmented on a beryllium target. The A1900 fragment separator contained an acrylic wedge degrader at the intermediate image. The momentum acceptance of the A1900 was limited to 1%. Details of the production of the secondary beams of $^{24}$F, $^{25}$F and $^{26}$F are listed in Table I.

At the final focus of the separator a stack of silicon detectors was located as shown in Figure 1. The stack consisted of three 500 $\mu$m thick silicon surface barrier detectors followed by three 5000 $\mu$m thick lithium-drifted silicon-diodes. A secondary 146 mg/cm² thick $^{12}$C target was located following the first silicon detector (#0). The...
TABLE I: Parameters for the three secondary fluorine beams: Average beam current ($< I >$), beamtime on target ($T$), primary target (beryllium) and wedge (acrylic) thickness, magnetic rigidity of the first ($B_{ρ1,2}$) and second ($B_{ρ3,4}$) set of the A1900 dipoles, and the energy, intensity ($I^*(F)$) and purity of the secondary fluorine isotopes.

|    | $< I >$ | $T$ | Target | Wedge | $B_{ρ1,2}$ | $B_{ρ3,4}$ | Energy | $I^*(F)$ | Purity |
|----|---------|-----|--------|-------|------------|------------|--------|----------|-------|
| $^{24}$F | 20      | 610 | 587    | 971   | 3.6017     | 2.8442     | 46.7   | 82       | 24    |
| $^{25}$F | 114     | 1340| 587    | 971   | 3.7796     | 3.0511     | 50.4   | 6.7      | 24    |
| $^{26}$F | 220     | 1590| 376    | 1278  | 4.1451     | 3.2565     | 53.8   | 0.64     | 43    |

setup was equivalent to that used in the measurement of proton knock-out reactions of $^8$B and $^9$C [21]. The fluorine and oxygen isotopes were stopped in the first thick silicon detector (#3).

The incoming fluorine isotopes were uniquely identified by the energy loss in the first detector (#0) and the time of flight measured with respect to the cyclotron RF.

The oxygen isotopes were identified by their $\Delta E - E$ signals in the second (#2) and third (#3) detector after the carbon target with the additional condition that an energy loss corresponding to oxygen isotopes was deposited in the first $\Delta E$ detector (#1) following the target. A mass identification spectrum was generated according to [22]:

$$\text{Mass ID} \sim \ln(a\Delta E) + (a - 1)\ln(E + c\Delta E) - a\ln(300)$$

where $\alpha = a - b\Delta E/T$ and $T$ is the $\Delta E$ detector thickness in $\mu$m. The identification spectrum was calibrated with the small percentage of oxygen isotopes which were directly produced in the A1900 production target and transmitted to the focal plane. These isotopes did not contribute to a potential background for the actual knock-out data, because of the requirement that the knock-out events had to be cleanly identified as incoming fluorine isotope in the first silicon detector (#0). The values of the parameters $a = 1.7715$, $b = 0.2$, and $c = 0.5$, were within the range suggested in Ref. [22].

The parameter $a$ was the most sensitive to a clean mass separation with deviations of less than 0.5% resulting in significant improvements. This analysis method had previously already been applied to single proton knock-out reactions for neutron-rich carbon isotopes [23].

III. DATA ANALYSIS AND RESULTS

Figure 2 shows the populated oxygen isotopes following breakup reactions from $^{24}$F (top), $^{25}$F (center) and $^{26}$F (bottom). The Mass ID parameter was normalized according to $A = (\text{Mass ID})/5$. The small overall energy dependence of the calibration results in a small shift for the $^{26}$F data so that mass 24 occurs in channel 118 instead of channel 120. In addition to the one-proton knock-out to the ground-state, which is guaranteed because no bound excited states exist in these isotopes, several oxygen isotopes of lower mass are populated. These

FIG. 2: Oxygen isotopes populated in proton knock-out reactions from $^{24}$F (top), $^{25}$F (center) and $^{26}$F (bottom). The Mass ID parameter can be converted to the mass number by $A = (\text{Mass ID})/5$, see text. (Color online)
TABLE II: Cross sections for the population of oxygen isotopes following breakup reactions.

| X    | \(^{(24F,X)}\) | \(^{(25F,X)}\) | \(^{(26F,X)}\) |
|------|----------------|----------------|----------------|
|      | (mb)           | (mb)           | (mb)           |
| \(^{24}O\) | —              | 3.8±0.6       | 4.1±1.4        |
| \(^{23}O\) | 6.6±1.0        | 6.4±0.9       | 8.9±2.4        |
| \(^{22}O\) | 11.6±1.6       | 13.1±1.5      | 12.4±2.9       |
| \(^{21}O\) | 15.1±1.7       | 13.0±1.4      | 13.1±3.0       |
| \(^{20}O\) | 13.0±1.9       | 8.9±1.3       | 9.4±2.2        |

TABLE III: Spectroscopic factors \(C^2S\), single particle \((\sigma_{sp})\), calculated \((\sigma_{calc})\), and experimental \((\sigma_{exp})\) single proton knock-out cross sections. The cross sections are given in mb.

| Reaction | \(C^2S\) | \(\sigma_{sp}\) | \(\sigma_{calc}\) | \(\sigma_{exp}\) |
|----------|----------|-----------------|-------------------|-----------------|
| \(^{26F,23O}\) | 0.91     | 8.3             | 7.6               | 6.6±0.9         |
| \(^{25F,23O}\) | 0.96     | 8.1             | 7.8               | 3.8±0.6         |
| \(^{20F,25O}\) | 0.98     | 7.8             | 7.6               | <4.1±1.4        |

In addition, the uncertainty of the contribution from the background from reactions in the detectors is added in quadrature.

A. Direct One-Proton Knock-Out Reactions to \(^{23,24,25}O\)

The dominant configuration of the valence proton in the projectiles of \(^{24,25,26}F\) is \(\pi d_{5/2}\) according to the shell model and the actual spectroscopic factors to the ground states calculated in the universal sd (USD) interaction \[^{26}\] given in Table III are very close to unity. The listed single-particle cross sections for the removal of this \(d_{5/2}\) proton were calculated in the eikonal theory \[^{21,22,23}\]. Assuming that the nuclei \(^{23}O\) and \(^{24}O\) have no bound excited levels \[^{2}\], the measured inclusive cross section should correspond to the product of the single proton knock-out to the ground state and the spectroscopic factor. The single particle \((\sigma_{sp})\) and the calculated single proton knock-out cross sections \((\sigma_{calc})\) are compared to the experimental values \((\sigma_{exp})\) in Table III.

For this calculation the proton separation energies were taken to be 14.4, 15.0 and 16.1 MeV for \(^{24,25,26}F\), respectively. The \(rms\) matter radii were deduced from experimental interaction cross-sections \[^{5}\] as 3.20(4) \((^{23}O)\) and 3.19(13) fm \((^{24}O)\) for the core and 2.32 fm for the \(^{12}C\) target. An uncertainty of 0.1 fm in the radii translates into an uncertainty of 0.9 mb for the single-particle cross-section. The Woods-Saxon parameters for the calculation of the wave function for the relative proton-core motion were taken as the “standard set” of ref. \[^{13}\].

This work deals with neutron and proton states with separation energies up to 19 MeV and strongly suggests that the eikonal calculation furnishes absolute spectroscopic factors, \(i.e.\) relating to physical occupancies of the shell-model states. These, however, turned out to be systematically reduced by a factor 0.5–0.6 relative to a many-body shell model based on effective interactions \[^{13,22}\]. This effect has been attributed to contributions from the nucleon-nucleon interaction not contained in the standard shell model. Viewed in this light, and with experimental errors and theoretical uncertainties taken into account, the resulting theoretical cross sections agree well with the measured values.

The strong population of the \(^{23}O\) ground state in the \((^{24}F,^{23}O)\) reaction yields additional evidence that the...
usual shell-model calculations give a good description of nuclei in this region. In fact, even the simplest picture, that of the ground state of $^{23}\text{O}$ described as a $|05/2\rangle \otimes 1s_{1/2}$ configuration, gives a near-quantitative description, both of the present data and of the $^{23}\text{O}$ neutron knock-out reactions [8, 27]. The spin of $^{24}\text{F}$, although most likely $3^-$, is not essential for the argument, given that the proton in any case will be in the $0d_{5/2}$ state.

For the population of the ground state of $^{25}\text{O}$ in the proton knock-out from $^{26}\text{F}$ only an upper limit can be extracted because $^{25}\text{O}$ is unbound and decays to $^{24}\text{O}$. The ground state of $^{24}\text{O}$ can also be populated from the decay of excited states in $^{25}\text{O}$. Thus, the measured cross section of $4.1\pm 1.4$ mb correspond to a sum of the contributions from the decay of the ground-state and excited states of $^{25}\text{O}$ (see also Figure 3(c) and the following section).

**B. Population of Other Oxygen Isotopes**

The cross section for the population of other oxygen isotopes in these breakup reactions can only be estimated because several production mechanisms can contribute. In addition to the single-proton knock-out followed by subsequent neutron ejection, direct population of the ground state as well as bound excited states have to be taken into account.

Within the eikonal approach one can calculate the single-particle distribution due to contributions from the knock-out of protons from the $p$-shell. The spectroscopic strength distribution as calculated within the shell model using the universal sd (USD) interaction [24] is shown on the left side of Figure 3. The single-particle cross section calculated in the eikonal model depends on the effective proton separation energy which is the sum of the proton separation energy and the excitation energy of the specific state. The proton separation energies for $^{24}\text{F}$, $^{25}\text{F}$, and $^{26}\text{F}$ are 14.4 MeV, 15.0 MeV, and 16.1 MeV, respectively. Figure 3 shows that the proton-removal cross sections are very similar for the three fluorine isotopes. In order to extract the total proton-removal cross sections from the $p$-shell the spectroscopic distributions were folded with the excitation-energy dependent stripping cross section of Figure 3. The values for the $p$-shell proton-removal cross sections are 25.7 mb, 25.2 mb and 25.0 mb for $^{24}\text{F}$, $^{25}\text{F}$, and $^{26}\text{F}$, respectively, and are listed (p.$\sigma_{\text{calc}}$) in Figure 3.

These populations are located above the one-, two-, three-, and even the four-neutron evaporation channel. The decay branches to the individual neutron channels depend on the details of the excited states in these nuclei. As mentioned above other processes also contribute to the population of these channels, so that calculating these decay branches is not useful. The only quantitative statement that can be extracted from the present data is that the calculated $p$-shell proton-removal cross section should not exceed the summed cross section of the open neutron channels.

For the reaction ($^{24}\text{F},^{19}\text{O}$) the 1-n to 3-n channels have to be taken into account. The threshold for the 4-n channel ($^{19}\text{O}$) at 21 MeV is located above the population for the removal of protons from the $p$-shell. The sum of the cross sections for these three neutron decay channels (population of $^{22}–^{20}\text{O}$) as listed in Table H is

![Diagram](https://via.placeholder.com/150)
39.7±3.0 mb, which has to be compared to a total proton-removal cross section from the p-shell of 25.7 mb. These cross sections are also indicated in Figure 3.

The sum of the population of the 1-n to 3-n channel \((^{23}_{21}\text{O})\) in the reaction \((^{25}_{24}\text{F},^{24}_{24}\text{O})\) is 32.4±2.2 mb. This value is only slightly larger than the calculated proton-removal cross section of 25.2 mb. However, the threshold for the 4-n channel \((^{20}_{20}\text{O})\) is located at 17.1 MeV, which is below the highest energies of the distribution of p-shell proton removal so that it also could contribute.

The reaction \((^{26}_{24}\text{F},^{24}_{24}\text{O})\) has to be treated differently because \(^{25}\text{O}\) is unstable and thus the contribution from p-shell removal can not be distinguished from the removal of the \(d_{5/2}\) proton. The total calculated single proton-removal cross section from \(d\)- and \(p\)-wave knock-out is 32.6 mb. The open channels as indicated in Figure 3 are the 1-n through 4-n decay, which corresponds to a cross section of 38.5±5.0 mb. It might be even possible that the 5-n channel \((^{20}_{20}\text{O})\) with a separation energy of 17 MeV can contribute.

For all three reactions studied, the predicted p-shell removal cross sections are consistent with the measured populations of the open neutron decay channels.

It is interesting to note that the widely used empirical fragmentation model EPAX \(^{28}\) yields cross sections of the order of 10–20 mb for the population of these oxygen isotopes in agreement with the values listed in Table III.

The recent measurements of fragmentation of unstable neutron-rich oxygen isotopes also included single proton knock-out cross sections \(^{29}\). These measurements were performed at significantly higher energies (>500 MeV/nucleon) and yielded cross sections of ~20 mb. These measurements were not performed as close to the dripline as the current experiment and the populated nitrogen isotopes all had bound excited states, so a direct comparison to the present analysis is not possible. Only the reaction of the most neutron-rich projectile \(^{21}_{16}\text{O}\) populates a nucleus with no known bound excited states \((^{20}\text{N})\). Unfortunately no cross section is quoted for this reaction \(^{29}\).

IV. CONCLUSIONS

The results of the single-proton knock-out reactions were analyzed within the a theoretical approach combining many-body shell model and eikonal theory. The cross section for the reaction \((^{24}_{22}\text{F},^{24}_{21}\text{O})\) is consistent with a single particle description of these nuclei, while the cross sections for the reaction \((^{25}_{24}\text{F},^{24}_{24}\text{O})\) shows a suppression of ~50%. However, experiments with higher precision are necessary in order to infer a change of the structure. The knock-out reactions on \(^{24}_{16}\text{F}\) and \(^{25}_{16}\text{F}\) are special because of the non-existence of bound excited states in \(^{23}\text{O}\) and \(^{24}\text{O}\), respectively. The present method promises to be a powerful tool to extract spectroscopic information for nuclei at the very edge of the driplines because they typically do not have any bound excited states. Other nuclei will require more sophisticated experimental arrangements, including \(\gamma\)-ray coincidences.

V. ACKNOWLEDGMENTS

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