On Restricting Real-Valued Genotypes in Evolutionary Algorithms

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Abstract. Real-valued genotypes together with the variation operators, mutation and crossover, constitute some of the fundamental building blocks of Evolutionary Algorithms. Real-valued genotypes are utilized in a broad range of contexts, from weights in Artificial Neural Networks to parameters in robot control systems. Shared between most uses of real-valued genomes is the need for limiting the range of individual parameters to allowable bounds. In this paper we will illustrate the challenge of limiting the parameters of real-valued genomes and analyse the most promising method to properly limit these values. We utilize both empirical as well as benchmark examples to demonstrate the utility of the proposed method and through a literature review show how the insight of this paper could impact other research within the field. The proposed method requires minimal intervention from practitioners and behaves well under repeated application of variation operators, leading to better theoretical properties as well as significant differences in well-known benchmarks.

Keywords: evolutionary algorithms · bounce-back · real-value · restricting · genome

1 Introduction

Evolutionary Algorithms (EAs) are a class of optimization algorithms that take inspiration from nature [6]. By taking inspiration from biological concepts such as hereditary traits, genotype - phenotype distinction, mutation, and survival of the fittest, EAs have been used to solve many challenging problems [3]. Many different encodings can be used to implement a genotype [17], among them is the real-valued genotype — a vector in R^n [8]. One often overlooked aspect of real-valued genotypes is the necessity to restrict the values to task specific bounds [19]. Restricting the values is fundamental since very few problems have infinite domains and because restrictions makes the search space feasible to explore [18].

In this paper, we demonstrate the challenges of restricting real-valued genotypes and the effect these limitations have on the distribution of values in the genome. We start by introducing the theoretical problem and how restriction
Clamping:

![Clamping Diagram](image)

Bounce-back:

![Bounce-back Diagram](image)

Fig. 1. By clamping the values in a real-valued genome the values will tend towards the limits of the bounds. The proposed Bounce-back function reflects values that exceed the limits back inside the bounds, resulting in a uniform distribution inside the bounds.

can affect the distribution. We then show that this problem is not simply a theoretical possibility; by optimizing benchmark functions we show that results diverge by solely varying the restriction function. We also look at the literature to gain an impression of how this problem could affect other EAs practitioners.

The contribution of our paper is a better understanding of how value restriction affects real-valued genotypes in EAs. In addition we show that this is a topic deserving of more scrutiny by the wider EA community through a literature overview of both well known EA frameworks and a review of conference proceedings. By showing both the theoretical as well as the practical side of this challenge, we hope that other researchers become aware of the need for better restriction functions for real-valued genotypes and can utilize the results presented here in future research.

2 Background

When designing a restriction function for real values, it is intuitive to create some form of a clamp method which ensures that a value does not exceed desired bounds. In the literature few articles have been dedicated to understanding the effect a restriction function could have on the evolutionary process. In [1] the authors compare different restriction methods on the result of evolving with Differential Evolution (DE) and showed that the results are impacted by the choice of restriction function. The paper [19] extended on this work by understanding which type of inheritance model functioned with different restriction functions.

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3 Like the ‘Clamp’ method introduced in .NET Core: [https://docs.microsoft.com/en-us/dotnet/api/system.math.clamp?view=netcore-2.0](https://docs.microsoft.com/en-us/dotnet/api/system.math.clamp?view=netcore-2.0) - accessed 18.05.2020
and as a by-product illustrated how these different restriction functions can alter
the search landscape. A larger review of different components that contribute
to the evolutionary process in DE were undertaken in [18], in this review article
the authors showed that the choice of restriction function can have a significant
impact on the results, a result backed by a very comprehensive comparison on
different benchmark functions. However, even with these articles, that show sig-
ificant impact on results solely on the basis of the restriction function, it is our
impression that few EA practitioners heed these warnings and make appropriate
accommodations in regards to restricting real-valued genotypes.

To gain insight into the practises of restricting real-valued genotypes within
the wider EA community, we conducted a limited literature review. We first be-
gan with identifying some of the larger open-source frameworks for implementing
EAs to see how value restriction is implemented.

DEAP [6] is one of the more popular Python based frameworks for imple-
menting EAs. Looking through the source code of this framework, two functions
implement genome value restriction, ‘cxSimulatedBinaryBounded’ and ‘mutPoly-
nomialBounded’. Both of these functions utilizes the Clamped function to limit
real-valued genomes. SFERESv2 [13] is another well known framework imple-
mented in C++. It too implements value restriction for real-valued genotypes as
can be seen in the genotype definition in ‘evo_float.hpp’. The restriction function
is implemented in ‘put_in_range’ and is equivalent to the Clamped function. Both
of these frameworks cite the same source when it comes to their implementation
of real-valued genomes and restriction, NSGA-II, a widely used Multi-Objective
Evolutionary Algorithm [4]. Consulting the source-code of this algorithm, it can
be seen that this too implements restriction through the Clamped function.

To evaluate whether or not the observations about evolutionary frameworks
are representative for the community, we conducted a small review of the main
proceedings from GECCO 2019 and the 2019 and 2020 EvoAPPS proceedings.
To evaluate if the results of a paper could be susceptible to the challenges, identi-
fied in this paper, we first identified experiments utilizing real-valued genotypes[6]
we then tried to identify if the authors discuss their strategy for value restric-
tion or if anything could be discerned from the source of the experiments. The
summary of our results can be seen in Table 1.

Table 1. Overview of real-valued genomes and limitation function in previous conference main proceedings.

|                | GECCO’19 | EvoAPPS 2019 | EvoAPPS 2020 |
|----------------|----------|--------------|--------------|
| Total number of papers | 173      | 42           | 44           |
| Uses real-valued genotype | 37 (21%) | 11 (26%)     | 10 (22%)     |
| Comments on value restriction | 4        | 3            | 1            |

Based on citations.
5 Source code available here: [http://www.iitk.ac.in/kangal/codes.shtml](http://www.iitk.ac.in/kangal/codes.shtml) - accessed 06.04.2020.
6 Note that papers utilizing Particle Swarm Optimization were excluded.
From the overview, we can see that real-valued genotypes are used in a large fraction of papers in these previous conferences. However, of those that could be identified to use some form of restriction only four papers in GECCO’19, three papers in EvoAPPS 2019 and one paper from EvoAPPS 2020 were found. Of the four papers in GECCO’19 two used strategies that can mitigate the challenges identified in this paper [7,14], with one of those being our contribution, while the other two papers used the Clamped function. Of the three papers identified in EvoAPPS 2019 two would not be affected, one not using Gaussian mutation [10], another is our previous contribution using the methods proposed here [15], while the last one used the Clamped method. From EvoAPPS 2020, one paper was identified to not be susceptible [16] by only using uniform random mutation between allowable bounds instead of Gaussian mutation.

3 Methods

Several possible functions can be devised for limiting individual genes in real-valued genotypes [1]. The easiest and most straightforward limitation function is to clamp the value to the given bounds. The function is defined as follows

\[
\text{clamp}(v, \text{min}, \text{max}) = \begin{cases} 
\text{min} & \text{if } v < \text{min} \\
\text{max} & \text{if } v > \text{max} \\
v & \text{otherwise}
\end{cases}
\]  

(1)

where \(v\) is the value to limit and \([\text{min}, \text{max}]\) are the bounds to apply for the value. This function will be used as the baseline to compare against the proposed Bounce-back method as it can be seen as the default when limiting real numbers[7] and is the only one implemented in the EA frameworks reviewed. We will refer to this function as Clamped for the remainder of this text.

The proposed limit function, which we will call Bounce-back restriction (also known as reflection [1]), is defined as follows

\[
\text{bounce-back}(v, \text{min}, \text{max}) = \begin{cases} 
\text{min} + (\text{min} - v) & \text{if } v < \text{min} \\
\text{max} - (v - \text{max}) & \text{if } v > \text{max} \\
v & \text{otherwise}
\end{cases}
\]  

(2)

where, again, \(v\) is the value to limit and \([\text{min}, \text{max}]\) are the bounds to apply for the value. The effect of the Bounce-back function is to redirect out-of-bounds values by the amount that the value is outside of the limits. The effect is illustrated in Figure 1. The function is independent of both mutation and crossover operators and can be applied in-between or after variation to ensure the genome is within given bounds. Compared to other restriction functions, such as wrapping, re-initialization and re-sampling [1], the Bounce-back function results in values

\[\text{Method included in C++17: https://en.cppreference.com/w/cpp/algorithm/clamp} \quad \text{- accessed 15.04.2020}\]
in the current vicinity of the solution while also having minimum computational impact.

One thing to note about the *Bounce-back* function, as defined in Equation 2, is that it is not guaranteed to result in values within the given bounds. This can happen when the value $v > \max + (\max - \min)$ or $v < \min - (\max - \min)$. This can either be solved by continued application of the restriction function until the value is within bounds or limiting the difference in Equation 2 with the *Clamped* function. The later solution was utilized when limiting the distribution in Figure 2.

To demonstrate the unwanted properties of the *clamp* function and how these properties are not present in the *Bounce-back* function, we will first take an empirical approach to restricting real-valued genotypes with Gaussian perturbation.

### 4 Empirical analysis

To understand why using the *clamp* function with real-valued genomes can be problematic we will begin by looking at how the function affects the Gaussian distribution. In Figure 2, the result of applying the two limiting functions to the Gaussian distribution is shown. The grey area shows the original Gaussian distribution while the colored areas represent the respective limitation functions as applied. This example is akin to mutating a value that is on or near the bound with Gaussian perturbation before restricting the value to be less than the bound. As can be seen from the figure, the *Bounce-back* function result in a distribution that is equivalent with the Gaussian distribution. Applying the clamping function results in a distribution that is heavily biased towards the ‘limit’. This shows the problem with simply clamping a value to the desired bounds, the value will be skewed towards the bounds because all values above the limit is restricted to become exactly the limit, as illustrated in Figure 1.

**Algorithm 1** Simulating mutation and value restriction of real-valued genotypes. ‘restrict’ is either the *Clamped* or *Bounce-back* function.

```plaintext
1: input $n$ \hfill▷ Number of values in genome
2: input $cycles$ \hfill▷ Number of times to simulate mutation
3: input $\sigma$ \hfill▷ Standard deviation of Gaussian perturbation
4: $genome_0 \leftarrow \mathcal{U}(0, 1)^n$ \hfill▷ Create a vector of $\mathbb{R}^n$, uniformly distributed
5: for $n \leftarrow 0$ to $cycles$ do
6:     for $i \leftarrow 0$ to $n$ do
7:         $genome_i \leftarrow \mathcal{N}(genome_i, \sigma)$ \hfill▷ Apply Gaussian mutation
8:         if $genome_i < 0.0$ or $genome_i > 1.0$ then
9:             $genome_i \leftarrow restrict(genome_i)$ \hfill▷ Apply restriction, if outside bounds
10:     end if
11: end for
12: end for
13: return $genome$
```
Fig. 2. The resulting distributions of applying the limit functions to a Gaussian distribution, in grey, with mean equal to the ‘limit’ value marked with a dashed line. This is analogous to mutating a value at ‘limit’ with Gaussian mutation and then restricting the value to be less than the ‘limit’. The Bounce-back distribution follows the Gaussian distribution while the Clamped distribution is skewed towards the ‘limit’.

To visualize how the two limitation functions will affect a real-valued genome we created Algorithm 1 which simulate how repeated application of Gaussian perturbation and restriction creates different distributions of values dependent on the limit functions. Figure 3 shows the distribution of values after running Algorithm 1 with \( n \) equal to 50000, cycles set to 100 and \( \sigma = 0.1 \). In the figure it can be seen that the distribution of the Clamped function is heavily skewed towards the bounds while the Bounce-back function has a much more uniform distribution.

To ensure that the distribution of the Bounce-back limitation is uniformly distributed, we performed a One-sample Kolmogorov-Smirnov test comparing the two distributions in Figure 3 with a uniform distribution. The results show that the Clamped distribution is statistically significant different from a uniform distribution, \( p \ll 0.05 \), while the Bounce-back distribution is not significantly different, \( p > 0.1 \).

To understand how the input parameters of Algorithm 1 impact the output, we varied the two parameters, cycles and \( \sigma \). We will postulate that the number of reals, \( n \), will not impact the underlying distribution and the effect of changing this parameter is to give a better or worse impression of the underlying distribution. The results of changing the input parameters are shown in Figure 4 and Figure 5 for number of cycles and varying the standard deviation respectively. Changing the number of cycles, shown in Figure 4, does not have an effect on the resulting distribution which is as expected. Since the probability of the Gaussian mutation going out- or staying inside the bounds is symmetrical, the number of times mutation is applied should not effect the resulting distribution. For the
standard deviation, shown in Figure 5, the results are slightly different. Here we can see an effect of increasing $\sigma$, which can be explained as a larger part of the initial uniform distribution having a probability of going out of bounds. For the Clamped function this results in more values restricted at the bounds as the standard deviation of the mutation increases. On the other hand, we can see that the Bounce-back function is not affected by changes in mutation and continues to be uniformly distributed.

5 Benchmark functions

To illustrate the potential impact of the limitation function, we applied the two limitation functions to a selection of benchmark problems [20]. All functions were optimized with a single objective ($\mu + \lambda$) EA using tournament selection, Gaussian mutation, and no crossover operator. The benchmark problems are included to illustrate the challenge of limiting the genome to a specific range outside of theoretical considerations, as demonstrated in the previous section.

The following four functions are used as benchmark problems:

\[
\frac{1}{4000} \sum_{i=1}^{N} x_i^2 - \prod_{i=1}^{N} \cos \left( \frac{x_i}{\sqrt{i}} \right) + 1
\]

(3)

\[
10N + \sum_{i=1}^{N} x_i^2 - 10\cos \left( 2\pi x_i \right)
\]

(4)
Fig. 4. A comparison of how the number of repetitions of the perturbation-limitation cycle affects the resulting distribution. The distribution in the figure were generated from 1000 uniform random values and perturbed by a Gaussian with $\sigma = 0.1$.

Fig. 5. A comparison of how the standard deviation, $\sigma$, of the Gaussian affects the resulting distribution. The distribution in the figure were generated from 1000 uniform random values and perturbed 100 times.
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\[
N-1 \sum_{i=1}^{N} (x_i^2 + x_{i+1}^2)^{0.25} \ast \sin^2 (50 \ast (x_i^2 + x_{i+1}^2)^{0.10} + 1) 
\]

\[
418.9828872724339 \ast N - \sum_{i=1}^{N} x_i \sin \left( \sqrt{|x_i|} \right) 
\]

where \( N \) is the size of the genome and \( x_i \) is the value of gene \( i \) in the genome. We will refer to equation (3) as Griewank, equation (4) as Rastrigin, equation (5) as Schaffer and equation (6) as Schwefel. The genotype was encoded as a vector of reals with a range of \([0,1]\), before being transformed into the range required by each benchmark task. Genotypes are randomly initiated based on a uniform distribution. To generate data, we first optimized the parameters for each function, selecting the best mutation rate \( \sigma \), tournament size and probability of applying Gaussian mutation to gene \( i \) - \( P(M|i) \). The final parameters used to generate data are shown in Table 2.

Table 2. Algorithm parameters for each benchmark function. Parameters marked with ‘†’ were taken from 2.

|                  | Griewank | Rastrigin | Schaffer | Schwefel |
|------------------|----------|-----------|----------|----------|
| Generations†     | 2000     |           |          |          |
| \((\mu + \lambda)\)† | 100 + 100 |           |          |          |
| Size - \( n \)†  | 30       |           |          |          |
| Repetitions      | 50       |           |          |          |
| Tournament       | 10       |           |          |          |
| \(P(M|i)\)       | 0.05     |           |          |          |
| Mutation - \( \sigma \) | 0.005  | 0.05     | 0.05    | 0.2     |
| Range            | ±600     | ±5.12    | ±100    | ±500    |

Figure 6 shows the mean and 95% confidence interval of the population minimum for each benchmark function. Statistical significant differences between the two limitation functions are marked in black at the bottom of each plot and is the result of applying the Wilcoxon Rank Sum test on intervals of 10 generations. To correct the p-value for the number of successive tests performed per row, Holm correction [9] was applied. The result show that only one benchmark function is sufficiently affected to lead to different results, however, both Rastrigin and Schaffer show diverging results at some points before converging. Based on the individual search parameters, shown in Table 2 we can also observe that larger \( \sigma \) seems to induce larger differences.

6 Discussion

From the empirical analysis performed, it can be seen that the Clamped function skews the distribution of values towards the bounds of the range, as shown in
Fig. 6. The mean and 95% confidence interval for the population minimum aggregated over 50 runs of each benchmark function. Differences are marked at the bottom of each graph in black, the difference is statistical significant using a Wilcoxon Rank Sum test over an interval of 10 generations adjusted for the number of tests using Holm correction.
Figure 2 and Figure 3. This property can be challenging when the genotype is based on real values that are translated into task applicable ranges during the phenotype conversion. The proposed Bounce-back function did not exhibit these properties resulting in no alteration of the underlying value distribution. When experimenting with different facets of mutation, Figure 4 and Figure 5, it was shown that the magnitude of the standard deviation had the most effect on the resulting value distribution. This can be understood as expanding the range of the Gaussian distribution applied at each value. As more values have the potential of being mutated near the bounds, more values will be restricted and end up at the extremities of the limit with the Clamped function. This leads to the observation that using a larger standard deviation in the mutation operator require more careful thought to which restriction function to apply.

The results in Figure 6 shows that the choice of restriction function can have an effect on benchmark problems, and is not just a theoretical problem. The effect of the restriction function followed closely the magnitude of the standard deviation used for mutation, detailed in Table 2, and illustrates the challenge that it can be difficult a priori to know the effect of the restriction function on any given task. One thing to point out about the benchmark tasks is that, except for Schwefel, the target value for all genes is $x_i = 0$, which is in the middle of the range, away from the bounds. As the target value moves closer to the bounds, we would expect the effect of the restriction function to grow, which could also explain the larger difference observed with the Schwefel benchmark function. With real-world tasks where the optimal value is difficult or impossible to confirm, it is even more challenging to a priori predict the effect and interactions of the restriction function, making it paramount that the restriction function has minimal impact on the optimization process.

The literature review conducted showed that two popular EA frameworks utilizes the Clamped function for restriction, and that while many papers published at GECCO’19 and EvoAPPS 2019 and 2020 utilized real-valued genotypes, few papers discussed their use of restriction functions. A deeper dive into the source of NSGA-II, a foundational algorithm within the Multi-Objective Evolutionary Algorithm literature, also revealed the use of the Clamped function which could affect re-implementations. Although limited, the literature review does underscore how the findings in this paper could impact the broader research field. As shown previously, the restriction function is not guaranteed to lead to significantly different results, however, it is difficult to predict the effect beforehand.

The results shown in this paper has focused on restricting real-valued genotypes in EAs. One interesting direction to take this work in the future is to apply the same Bounce-back technique on particles in Particle Swarm Optimization (PSO) [11]. Because of the additional velocity attribute present in PSO the restriction function should take this into account when limiting so that the particles do not keep moving towards the bounds. In the same vein, it would be interesting to know if PSO is sensitive to the challenges presented in this paper, or if the collective behavior can mitigate the boundary effect shown in this paper.
7 Conclusion

In this paper we have shown that one of the most used functions for restricting real-valued genotypes behaves badly under repeated application of the variation operators. We therefore suggest a different function which result in a uniform distribution of values within the genome. The Bounce-back function is shown both empirically and in practise to lead to better distributions and requires minimal intervention from existing [Evolutionary Algorithm] implementations, while having a minimal computational impact. We also conducted a limited literature review which illustrated that other practitioners in the field of [Evolutionary Algorithm] could be susceptible to the complications detailed in this paper. We hope that by illuminating this problem other researchers will become aware of the requirements for restricting real-valued genotypes, and can hopefully mitigate it with minimal effort in future work.

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