Forecast of China's Future Population under the Universal Two-child Policy

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Abstract: Firstly, according to the total population of China from 1996 to 2015 collected and sorted, the curve function was fitted using MATLAB tools and the polynomial difference method. According to the function predicted by the fitting function, the population of China in 2016 was 1.769.8 billion under the premise of no open two-child policy. Secondly, the functional relationship between mortality rate and time was obtained by using MATLAB tools and least squares algorithm, logistic model and curve fitting. Therefore the mortality rate in 2016, as well as the future mortality rate of China's population was predicted. Finally, a differential equation model and recursive mode were set up. Under the assumption that the birth rate of approximately equal to 1.2916% per year, generation into the prediction model, it is concluded that under the universal two-child policy in our country in 2016 and the total population of about 1.38242 billion people, the result that tallies with the China's population will reach 1.385 billion in 2016, and its forecast effect is better. At the same time, the annual population of China is predicted for the next ten years.

1. Introduction

China is a big country with a population of 1.3 billion. The population problem will inevitably directly affect the development of social economy. From the initial implementation of family planning to the gradual opening of the birth policy, to the "universal two-child" policy, China's population and natural growth rate are constantly changing, and the demographic structure also presents different characteristics. Nowadays, the implementation of the "universal two-child" policy in the serious situation of an aging population structure, a prosperous old age and a serious minority child will inevitably lead to a rapid increase in the number of newborns in China. But there is no first-hand data in the national census. It is necessary to construct a prediction model for the future population, and implement the algorithm by combining the future population mortality rate obtained from the prediction of China's future population under the policy of “universal two-child”.

2. China's population forecast before the policy of “universal two-child”.

According to the relevant data of the total population of China in the past 20 years provided by the National Bureau of Statistics, and the future population of China is predicted when the policy is not open by using the MATLAB software tool and curving fitting in the polynomial difference method. China's population in 1996-2015 is shown in Table 1.

| Year | 1996 | 1997 | 1998 | 1999 | 2000 | 2001 | 2002 | 2003 | 2004 | 2005 |
|------|------|------|------|------|------|------|------|------|------|------|
| Total number of people (10,000) | 122389 | 123626 | 124761 | 125786 | 126743 | 127627 | 128453 | 129227 | 129988 | 130756 |
| Year | 2006 | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 | 2013 | 2014 | 2015 |
| Total number of people (10,000) | 131448 | 132129 | 132802 | 133450 | 134091 | 134735 | 135404 | 136072 | 136782 | 137462 |

The above data was processed by MATLAB software and EXCEL to make a scatter plot of the population of China, shown in Figure 1, in preparation for the later comparative analysis.
From the chart, it can be seen that in order to improve the prediction accuracy and reduce the
error, the prediction of China's population under the policy of not fully opening the second child can
be determined by polynomial regression analysis, and combined with the paired t test to enhance the
prediction accuracy.

2.1 Polynomial regression analysis

A polynomial regression analysis of a dependent variable and one or more independent variables
is called polynomial regression [1].

In the one-way regression analysis, if the relationship between variables exhibits a nonlinear and
complex feature, a one-dimensional polynomial regression can be used. A one-dimensional
polynomial regression equation is established.

\[ S(x) = a_0 + a_1x + a_2x^2 + \cdots + a_nx^n \]

2.2 Least squares algorithm

Finding the curve function with the smallest sum of squared errors in the data and observation
data is called the least squares fit. In geometric language, it is called the least squares method of
curve fitting [2].

(1) Based on the observed data, assume the form of the functional relationship. \( S(x) \) is a linear
form. If \( \varphi_i(x) \) it is a polynomial, \( S(x) \) is a polynomial, as shown below.

\[ S(x) = a_0\varphi_0(x) + a_1\varphi_1(x) + \cdots + a_n\varphi_n(x) \quad (n < m) \]

(2) Establish a weighted sum of squared errors:

\[ \|\delta\|^2 = \sum_{i=0}^{m} \omega(x_i)[S(x_i) - f(x_i)]^2 \]

(3) Determine the least squares error:

\[ \|\delta\|^2 = \sum_{i=0}^{m} \delta_i^2 = \sum_{i=0}^{m} [S^*(x_i) - y_i]^2 = \min_{S(x) \in \mathcal{F}} \sum_{i=0}^{m} [S(x_i) - y_i]^2 \]

Which is to ask for a function \( y = S^*(x) \). Make the minimum, it translates into a multivariate
function,

\[ I(a_0, a_1, \cdots, a_n) = \sum_{i=0}^{m} \omega(x_i) \left[ \sum_{j=0}^{n} \varphi_j(x_i) - f(x_i) \right]^2 \]

The problem of the minimum value of the function, the necessary conditions for finding the
extremum of the multivariate function are,
\[
\frac{\partial I}{\partial a_k} = 2 \sum_{i=0}^{m} \omega(x_i) \left[ \sum_{j=0}^{m} a_j \varphi_j(x_i) - f(x_i) \right] \varphi_k(x_i) = 0 \quad (k = 0, 1, \ldots, n)
\]

(4) Establish a regular equation system: \( \sum_{j=0}^{m} \left( \varphi_k, \varphi_j \right) d_j = 0 \quad (k = 0, 1, \ldots, n) \)

Among them, to make the equation have a unique solution, there are:

\[
\begin{bmatrix}
(\varphi_0, \varphi_0) & (\varphi_0, \varphi_1) & \cdots & (\varphi_0, \varphi_n) \\
(\varphi_1, \varphi_0) & (\varphi_1, \varphi_1) & \cdots & (\varphi_1, \varphi_n) \\
\vdots & \vdots & \ddots & \vdots \\
(\varphi_n, \varphi_0) & (\varphi_n, \varphi_1) & \cdots & (\varphi_n, \varphi_n)
\end{bmatrix} = 0
\]

Solving through the equations, finally the most suitable curve function relationship is found.

2.3 Algorithm application

(1) Model establishment
   Assume that the population function function in China is:
   \[ y = a_0 t^3 + a_2 t^2 + a_1 t + a_0 \]

(2) Raw data preprocessing \[^3\]
   Considering that the units of the data are inconsistent, the data in the table is preprocessed first. The preprocessing formula is shown in Equation.
   \[ \frac{\lambda - \lambda_{\text{min}}}{\lambda_{\text{max}} - \lambda_{\text{min}}} \]

(3) Curve fitting
   Using MATLAB software to program the fit \[^4\], the relationship between the total population and time is shown in Equation.
   \[ y = 0.0001 t^3 - 0.0046t^2 + 0.1312t + 12.1171 \]
   Its fitting curve is shown in Figure 2.

![Figure 2 Population population fit curve](image)

(4) Paired t-test \[^5\]
   Assumption: \( H_0 : \mu_0 = 0 \). The difference between the function value and the experimental data is zero.
   Assumption: \( H_0 : \mu_0 \neq 0 \). The difference between the function value and the experimental data is not zero.
(5) Population forecast
If \( x = 21 \), it is predicted that the population of 2016 will be 137.698 million people without the policy of opening two-child policy.

3. China’s future population mortality forecast

A Logistic relationship model between death population and time was established. Through the curve fitting, the separable variable method was used to predict the annual mortality rate of China in the future.

Through the compilation of the National Bureau of Statistics' 1996-2015 China Population Mortality Release Data, MATLAB software was used to make a scatter plot of population mortality rate about time in China \([6]\), shown in Figure 3.

![Figure 3 scatter diagram of China's population mortality from 1996 to 2015](image)

It can be seen from the intuitive picture that the mortality rate of the Chinese population increased from 1996 to 2015 with the increase of the year, but after increasing to a certain extent, the growth rate gradually slowed down. It can be predicted that the fitting curve of this data is s-type curve, so the retarded growth Logistic model can be used for the forecast analysis.

3.1 Introduction to Logistic model

The Logistic model is an important mathematical model proposed by Dutch mathematical biologist Ve Rhuist in 1938 to study the growth law of biological population in limited space \([7]\). Ecologists have used it to simulate and describe the growth process of various biological populations, and it has been widely used in similar fields.

Its basic form is shown in Equation.

\[
\begin{align*}
\frac{dx}{dt} &= rx(t) \left(1 - \frac{x(t)}{N}\right) \\
x(0) &= 0
\end{align*}
\]

Where, \( x(t) \) represents the population quantity at any time, \( r \) is the intrinsic growth rate (i.e. the growth rate minus the mortality rate) of China’s population, and \( N \) is the maximum population that the environment can accommodate.

3.2 Use the separable variable method to solve

The separable variable method in ordinary differential equation is applied to solve the equation.

\[
x(t) = \frac{N}{1 + \left(\frac{N}{x(0)} - 1\right)e^{-rt}}
\]
3.3 Demographic mortality prediction analysis

First, establish the Logistic model: \[ r_0 = \frac{1}{1 + ae^{kt}} \]

Secondly, simplify by using the logarithm method shown in Equation.

\[ \ln\left(\frac{1}{r_0} - 1\right) = \ln a + kx, \quad R = \ln\left(\frac{1}{r_0} - 1\right), \quad A = \ln a, \]

The unary linear regression model can be obtained: \( Y = kx + A \).

Finally, using MATLAB software programming, the solution is: \( k = -0.0068 \), \( A = 5.0621 \). The Logistic model of mortality is shown in Equation.

\[ r_0 = \frac{1}{1 + e^{5.0621 - 0.0068x}} = \frac{1}{1 + 157.9218e^{-0.0068x}}, \]

The specific image is obtained and shown in Figure 4.

![Figure 4 China's population mortality curve from 1996 to 2015](image)

Thus, data of China's future mortality rate in 2017-2030 can be predicted, shown in Table 2.

| year  | 2017   | 2018   | 2019   | 2020   | 2021   | 2022   | 2023   |
|-------|--------|--------|--------|--------|--------|--------|--------|
| mortality(%) | 0.69711 | 0.68832 | 0.67785 | 0.6657  | 0.65184 | 0.63636 | 0.61917 |

| year  | 2024   | 2025   | 2026   | 2027   | 2028   | 2029   | 2030   |
|-------|--------|--------|--------|--------|--------|--------|--------|
| mortality(%) | 0.6003  | 0.57975 | 0.55752 | 0.53361 | 0.50822 | 0.48075 | 0.4518 |

4. The opening-up policy

The differential equation and the recursive model are established, and a comparative analysis of China's population in the future is made under the policy framework of "universal two-child policy".

4.1 Prediction of the differential equation model

It is known that population growth rate \( r \) is the difference between population birth rate \( r_1 \) and population death rate \( r_0 \). As the population growth is shown in Equation.

\[ x(t + \Delta t) - x(t) = \Delta t x(t)(r_1 - r_0) \]

Therefore, the differential equation model is established and shown in Equation.
\begin{align*}
\begin{cases}
\frac{dx(t)}{dt} = x(t)(r_1 - r_0) \\
x(21) = x_0
\end{cases}
\end{align*}

It is known that 17.86 million people were born in 2016 and the total population is 137.698 million. The birth rate in 2016 can be obtained.

\[ r_1 = \frac{1786}{137698} \times 100\% = 1.2916\% \]

So
\[
\begin{align*}
\frac{dx(t)}{dt} &= x(t)\left[0.0129 - \frac{1}{1 + 157.9218e^{-0.0068t}}\right] \\
x(21) &= 137698
\end{align*}
\]

The general solution of the equation is obtained by the method of separating variables, shown in Equation.

\[ \ln x(t) = C - 0.9871t - \frac{\ln(1 + 157.9218e^{-0.0068t})}{0.0068} \]

A special solution:

Therefore, the prediction model of population size is shown in Equation.

\[ \ln x(t) = 757.0514 - 0.9871t - \frac{\ln(1 + 157.9218e^{-0.0068t})}{0.0068} \].

4.2 Prediction of recursive model

As it can be predicted from the above problems, the mortality rate of the population in 2016 is 0.7308%.

Total population in 2016 = total population in 2015 + number of births - number of deaths = 137462 + 1786 - 137698 × 0.7308% = 1382420000.

This result is consistent with Tan Yong Hong's [9] prediction that the total population of China will reach 1.385 billion in 2016.

After comparison and analysis, the prediction results of the recursive model are more ideal. Therefore, it is assumed that after the full implementation of the two-child policy, the annual fertility rate is,

\[ b(n) = 1.2916\% \]

According to the population recurrence relations shown in Equation.

\[ y(n+1) = y(n) + y(n+1)[b(n+1) - d(n+1)] \].

The recursion model of total population established is shown in Equation.

\[ y(n+1) = \frac{y(n)}{[1 - b(n+1) + d(n+1)]} \]

By using this model and MATLAB software programming, the total annual population of China in 2017-2030 can be predicted, shown in Table 3.
Table 3 China's annual population in 2017-2030

| year    | 2017   | 2018   | 2019   | 2020   | 2021   | 2022   | 2023   |
|---------|--------|--------|--------|--------|--------|--------|--------|
| Total   |        |        |        |        |        |        |        |
| number  |        |        |        |        |        |        |        |
| people  |        |        |        |        |        |        |        |
| (10,000)|        |        |        |        |        |        |        |
| year    | 2024   | 2025   | 2026   | 2027   | 2028   | 2029   | 2030   |
| Total   |        |        |        |        |        |        |        |
| number  |        |        |        |        |        |        |        |
| people  |        |        |        |        |        |        |        |
| (10,000)|        |        |        |        |        |        |        |

5. Summary

Based on the total population of China collected from 1996 to 2015 in this paper, the recursive model and the regression analysis model are established. By using the least squares algorithm, the Logistic model and curve fitting methods, the functional relationship between mortality and time is obtained. Thus, the annual mortality after 2016 is predicted, and finally the total population of China under the universal two child policy is predicted.

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