Supporting Information to: Hybrid Tip-Enhanced Nanospectroscopy and Nanoimaging of Monolayer WSe$_2$ with Local Strain Control

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POLARIZATION DEPENDENCE OF TIP PLASMON

Fig. S1a and b show experimental setup, and tip plasmon and WSe$_2$ PL spectra with respect to the incident polarization angle $\theta$ as defined in the inset. The incident beam is focused onto the tip apex, and the WSe$_2$ sample is initially located out of focus at 1 $\mu$m distance below the tip. The tip plasmon intensity is strong for $P_{\text{in}}$ excitation ($\theta = 150^\circ$) and substantially decreased (> 10 times) for $S_{\text{in}}$ excitation ($\theta = 60^\circ$). The far-field PL intensity of WSe$_2$ is not affected by the tip plasmon and the small change of intensity for the different angle results from the polarization dependent reflectivity of the beam splitter.

Figure S1. (a) Schematic of the multi-modal TEPL/TERS setup. EF: edge filter, BS: beam splitter, OL: objective lens. (b) Confocal far-field tip plasmon and WSe$_2$ PL spectra for three different polarization angles of incident laser.
DISTANCE-DEPENDENT TIP PLASMON AND PHOTOLUMINESCENCE

Fig. S2a shows tip-sample approach behavior. As the tip is closely approaching to the sample, the PL spectral intensity of WSe$_2$ is enhanced as shown in Fig. S2b due to near-field interaction. Notably, the tip plasmon is quenched in this regime (marked with white dashed box in Fig. S2a). This tip plasmon quenching can be possibly understood as a result of the optical excitation transfer from the tip to the WSe$_2$ with subsequent non-radiative decay. We find typical tip plasmon resonances in the range between 600 and 800 nm PL but not consistently for all gold tips used. However, for those tips which exhibit a tip plasmon resonance, we generally observe tip-enhanced PL of WSe$_2$.

![Figure S2](image)

Figure S2. (a) Tip-sample distance dependence of TEPL of monolayer WSe$_2$. Spectra are measured in 1.5 nm increments and 0.2 s acquisition time. (b) Amplitude changes of tuning fork and the peak intensity changes of tip plasmon and WSe$_2$ PL ($\sim$770 nm) with respect to tip-sample distance derived from the (a). (c) Tip plasmon and WSe$_2$ PL spectra for the different tip-sample distances (35 nm and 5 nm).

It should be noted that biexciton peak is emerged when the tip-enhancement factor is high enough as shown in Fig. 3d. Assignment of the high energy shoulder to biexcitons is suggested based on spectral position in comparison with other studies and the emergence of
that spectral feature only when the tip-enhancement is sufficiently high, as shown in Fig. 3d, suggesting the expected super-linear excitation intensity dependence. Specifically, the \(\sim 50\)–\(60\) meV separation between peaks is consistent with the energy difference between exciton and biexciton peaks as reported in the literature [1, 2]. Observation of biexcitons has been also reported in literature for CW excitation using 0.1 - 10 mW power, which translates into excitation intensities of \(10^4\) - \(10^6\) W/cm\(^2\) [3, 4]. In our experiment, for the incident intensity of \(10^5\) W/cm\(^2\), only a single exciton peak is observed in the far-field measurements (Fig. 1d). The appearance of an additional peak in the near-field, where the local excitation intensity can increase up to \(10^7\) W/cm\(^2\) due to the local field enhancement at the tip apex on the order of 10, seems consistent with the expected super-linear dependence of biexciton emission on excitation intensity [3, 4].
RAT**E EQUATION MODEL FOR TEPL AND TERS**

In order to describe the dependence of TEPL and TERS signals on the tip–sample distance $z$, we use rate equations for the excited state population of sample ($P_s$) and tip plasmon ($P_{tip}$) as described in [5]:

\[
\frac{dP_s}{dt} = \Gamma_e(z) - (\Gamma_s + \Gamma_{RET}(z)) P_s + \Gamma_{RET}(z) P_{tip},
\]

\[
\frac{dP_{tip}}{dt} = - (\Gamma_{tip} + \Gamma_{RET}(z)) P_{tip} + \Gamma_{RET}(z) P_s.
\]

Here, we take into account a spatially integrated, over the near-field probe area, distance-dependent excitation rate $\Gamma_e(z) \propto (1/(R+z))^4$, with tip apex radius $R$. Damping rates include radiative and non-radiative contributions $\Gamma_{s,tip} = \Gamma_{rad, s,tip} + \Gamma_{nrad, s,tip}$, and the non-radiative resonance energy transfer (RET) rate $\Gamma_{RET}(z) = \Gamma_{tip}^{rad}(R_0/z)^m$, with $m = 4$ due to the reduced dimensionality and the characteristic length scale of near-field energy transfer $R_0$.

We solve the equations for steady state and as a function of $z$, and obtain the PL intensity $I_{PL}(z) \propto \eta_{tip} P_{tip} + \eta_s P_s$, where $\eta_{s,tip} = \Gamma_{s,tip}^{rad}/\Gamma_{s,tip}$ is the quantum yield of the sample and tip emission.

As shown in Fig. 1e, a good agreement between the simulation and the experimental TEPL data is found for fit parameters with tip radius $R \sim 30$ nm, damping rates and quantum yields of $1/\Gamma_s \sim 0.5$ ps, $\eta_s \sim 0.1$, $1/\Gamma_{tip} \sim 30$ fs, $\eta_{tip} \sim 0.5$, and a RET length $R_0 \sim 8$ nm. TERS intensity is simulated using the same set of parameters, but assuming very short ($1/\Gamma_s \sim 5$ fs) lifetime of the excitation, to describe the near instantaneous character of the Raman process.
MULTIMODAL IMAGING

The monolayer (ML) WSe$_2$ has a PL peak at $\sim 772$ nm ($\sim 1.606$ eV) and the PL intensity is uniform across the crystal face region. The PL intensity is decreased in the center and edge region, and the peak position is blueshifted. To visualize the spatial heterogeneity of the PL spectrum, we plot integrated intensities for the main PL (770-805 nm) and the blueshifted PL (725-760 nm) spectrally integrated at each pixel of sample scanning as described in Fig. 2c (main text). In addition, we subtract the main PL image from the blueshifted PL image after compensating for intensity variation.

It should be noted that despite high spatial resolution TEPL images enabled by the strong localized plasmon effect (Fig. 2d-f), there is a superimposed weak homogeneous far-field background signal over micron length scale. Note also that it is difficult to obtain 15 nm resolution for large area scanning due to the different thermal expansion of tip and objective lens mounts, as well as overall drift of the scanner ($\sim 1$ nm/min) on the time scale of such a measurement. Although reproducible 50 nm spatial resolution images were obtained in the whole crystal scanning, the presented near-field image is a composite of several 1 $\mu$m $\times$ 1 $\mu$m or 2 $\mu$m $\times$ 1 $\mu$m TEPL image scans to achieve the best resolution images.

Fig. S3c shows line profiles for the 770 nm PL peak and 273 cm$^{-1}$ Raman mode (same data as Fig. 4f of main text). We estimated a spatial resolution of 15 $\pm$ 5 nm according to the general convention (distance between 5% and 95% of optical intensity at the step edge).

Figure S3. (a) Confocal PL image of the ML WSe$_2$ for the integrated intensity at 725-770 nm (blueshifted PL). Corresponding confocal PL image for the integrated intensity at 770-805 nm is shown in Fig. 2a. (b) Corresponding spectral difference confocal PL image. (c) Line profiles for the 770 nm PL peak and 273 cm$^{-1}$ Raman mode which exhibiting 15 $\pm$ 5 nm spatial resolution.
The change of direct bandgap energy of ML WSe$_2$ with respect to the applied tensile strain was calculated previously using the Heyd–Scuseria–Ernzerhof (HSE) density functional theory (DFT) [6]. The bandgap energy of ML WSe$_2$ is found to change linearly with the tensile strain. The PL peak of the unstrained sample depends on the growth condition and substrates. Our analysis is based on the assumption of the PL peak energy of the transferred WSe$_2$ crystal having 0% strain. The tensile strain of as grown sample is then calculated based on the linear dependence of the PL energy with strain as shown in Fig. S4 [6].

Figure S4. Calculation result for the bandgap change of ML WSe$_2$ with respect to the tensile strain. We assume the PL peak energy of the transferred sample has a 0% strain.
The atomic defects at the twin GBs of ML TMDs have been investigated with transmission electron microscopy (TEM) [7, 8]. These atomic defects of GBs can be further deformed or bonds broken under high strain as a result of the crystal growth procedure [7, 9]. We therefore suggest that in the previous far-field PL imaging studies, which showed clear PL decrease/increase at the GBs of the large size TMD crystal (> 10 µm), might measure structurally deformed GBs [7, 9]. The large TMD crystals might have particularly high strain effect due to the long growth time and result in significantly large areas of PL modification at GB region. On the other hand, since the small TMD crystals have much less strain effect, PL modification is constrained to the nanoscale areas possibly dictated by exciton diffusion at the mid-gap states. In order to address this hypothesis, we perform far-field confocal PL imaging (∼500 nm resolution) for ∼10 µm size polycrystalline WSe₂ crystal, and PL quenching at GBs is clearly revealed as shown in Fig. S5a-c. It should be also noted that despite the crystal sizes are small, interflake GBs always showed distinct PL quenching due to the structural deformation as shown in Fig. S5d-f.
Figure S5. (a) Optical microscopy image of a polycrystalline ML WSe$_2$. (b) Confocal PL image for the integrated intensity at 725-760 nm spectral range. (c) Confocal PL image for the integrated intensity at 770-805 nm spectral range. (d) Topography image of the polycrystalline WSe$_2$ with dislocated GBs. (e) TEPL image of interflake GB region (indicated in (d) as a white dashed box) for the integrated intensity at 725-760 nm spectral range. (f) TEPL image of sample region for the integrated intensity at 770-805 nm spectral range.

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