Overdensity of SMGs in fields containing \( z \sim 0.3 \) galaxies: magnification bias and the implications for studies of galaxy evolution

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ABSTRACT
We report a remarkable overdensity of high-redshift submillimetre galaxies (SMG), 4–7 times the background, around a statistically complete sample of twelve 250 \( \mu m \) selected galaxies at \( z = 0.35 \), which were targeted by ALMA in a study of gas tracers. This overdensity is consistent with the effect of lensing by the haloes hosting the target \( z = 0.35 \) galaxies. The angular cross-correlation in this sample is consistent with statistical measures of this effect made using larger sub-mm samples. The magnitude of the overdensity as a function of radial separation is consistent with intermediate scale lensing by haloes of the order of \( 7 \times 10^{13} M_{\odot} \), which should host one or possibly two bright galaxies and several smaller satellites. This is supported by observational evidence of interaction with satellites in four out of the six fields with SMG, and membership of a spectroscopically defined group for a fifth. We also investigate the impact of these SMG on the reported Herschel fluxes of the \( z = 0.35 \) galaxies, as they produce significant contamination in the 350 and 500 \( \mu m \) Herschel bands. The higher than random incidence of these boosting events implies a significantly larger bias in the sub-mm colours of Herschel sources associated with \( z < 0.7 \) galaxies than has previously been assumed, with \( f_{\text{boost}} = 1.13, 1.26, 1.44 \) at 250, 350, and 500 \( \mu m \). This could have implications for studies of spectral energy distributions, source counts, and luminosity functions based on Herschel samples at \( z = 0.2–0.7 \).

Key words: galaxies:haloes – gravitational lensing:weak – submillimetre:galaxies.

1 INTRODUCTION

The effect of gravitational lensing on our view of the distant submillimetre (sub-mm) sky has been known and exploited since the beginning of the era of sub-mm surveys. Lensing was originally seen as a tool for gaining information on the fainter end of the source counts, and surveys were targeted at massive clusters to benefit from the strong magnifications they produce (Smail, Ivison & Blain 1997; Blain et al. 1999; Cowie, Barger & Kneib 2002; Knudsen, van der Werf & Kneib 2008; Zemcov et al. 2010; Hsu et al. 2016).

In more recent years, strong lensing due to individual galaxies has also been exploited to reveal the high redshift dusty star-bursts in exquisite detail, with wide area FIR/sub-mm surveys producing large samples of such strongly lensed systems (e.g. Negrello et al. 2010; Vieira et al. 2010; ALMA Partnership et al. 2015; Cañameras et al. 2015; Swinbank et al. 2015; Negrello et al. 2017; Zhang et al. 2018; Jarugula et al. 2019; Yang et al. 2019).

The reason that lensing has been so helpful to sub-mm astronomy is that the conditions for producing lots of lensing signal in the population are optimal, with steep sub-mm source counts and the population of SMG predominantly residing at high redshifts. (e.g. Blain 1997; Negrello et al. 2007; Lapi et al. 2012). However, this boon from the lensing phenomena comes with a price for those simply interested in the statistics of the galaxy populations. Lensing is so ubiquitous that it must be considered a possibility that any SMG which has a luminosity \( L_{\text{IR}} > 10^{13} L_{\odot} \) is being lensed, even if the lens itself is not visible – either being too high redshift, or because the lensing is from intervening large scale structure such as a group or cluster (e.g. Rowan-Robinson et al. 1991; Graham & Liu 1995; Harris et al. 2012; Bussmann et al. 2015; Nayyeri et al. 2017).

Statistical analyses comparing the positions of high redshift sub-mm galaxies and lower redshift populations reported cross-correlation signals right from the earliest days, but with only marginal statistical significance given the small areas imaged (Almaini et al. 2005; Aretxaga et al. 2011; Wang et al. 2011). With the wide area submillimetre Herschel-ATLAS survey (Eales et al. 2010) and complementary optical spectroscopic survey from Galaxy and Mass Assembly (GAMA; Driver et al. 2011), a leap was made in the detection and characterization of this signal as being that of cosmological lensing bias: the lensing effect from the foreground large-scale structure on the background high redshift galaxy population (González-Nuevo et al. 2014, 2017). The lensing is not thought to be strong, with magnification factors of 1.0–1.5 but it nevertheless changes the statistics and potentially imprints the correlation function of the high-z galaxies with the signal from the lower redshift structures which are magnifying them.

The two regimes of lensing, strong (from clusters or single galaxies producing arcs, rings, or multiple images), and weak (from large-scale foreground structure which produces the cosmological lensing bias at large angular scales seen in Hildebrandt et al. 2013...
and González-Nuevo et al. (2014; González-Nuevo et al. 2017), are reasonably well recognized and understood. There is, however, a third regime intermediate between strong and weak which has only recently been identified, and which is the subject of this paper. This regime, spanning scales of a few arcsec to a few tens of arcsec, produces an upturn in the cross-correlation signal between low redshift populations and z > 1.5 SMG. Statistical evidence for this intermediate lensing regime has been highlighted in the angular cross-correlation study of H-ATLAS high redshift sources with low redshift optical galaxies (González-Nuevo et al. 2017). Pre-dating this study, it was also hypothesized as a possible explanation for a puzzling trend noted during the H-ATLAS cross-identification studies (Smith et al. 2011; Bourne et al. 2016) in which H-ATLAS sources with red sub-mm colours (aka high redshift) and SDSS optical galaxies had a broader cross-correlation peak in angular scale compared to H-ATLAS sources with blue sub-mm colours (aka low redshift) and the same SDSS optical galaxy catalogue (Bourne et al. 2014). Both statistical signals are thought to be due to the same effect: moderate lensing by haloes hosting galaxy groups or very massive centrals with a number of satellite dwarfs. The lensing is not strong enough to create distortions in the sub-mm images, but should have amplifications in the range $\mu = 1−3$ (González-Nuevo et al. 2017). The lensing occurs on scales similar to the profile of the large halo or group of haloes, so is at 3–15 arcsec rather than the < 3 arcsec expected for strong galaxy–galaxy lensing, or the >1 arcmin scales of weak lensing by the large-scale structure.

In this paper, we describe the serendipitous detection of a large overdensity of SMG within 13 arcsec of z = 0.35 galaxies. The galaxies were originally targeted by ALMA as a small, but homogeneously selected sample in the relatively local Universe, which could provide a calibration of gas tracers in dust, CO, and [CI]. We believe that this is a first detection of the intermediate lensing regime in individual sources.

In Section 2 we describe the sample, observations, and data reduction. In Section 3 we present the very surprising result that there is an overdensity of a factor 4–6 in the number of SMG found in these fields compared to blank field surveys. In Section 3.2 we investigate a lensing mechanism for this overdensity and in Section 4 we discuss the wider implications of flux boosting in Herschel surveys. Throughout we use a cosmology with $\Omega_m = 0.308$, $\Omega_{\Lambda} = 0.692$, and $H_0 = 67.8 \text{ km s}^{-1} \text{Mpc}^{-1}$ (Planck Collaboration XIII 2016).

### Table 1. Properties of the target $z = 0.35$ galaxies.

| H-ATLAS IAU | SDP name | GAMA ID | R.A. Dec. (hh:mm:ss.s dd:mm:ss.s) | z | $S_{250}$ (mJy) | $r_p$ (mag) | SMG |
|-------------|----------|---------|-----------------------------------|---|--------------|----------|-----|
| J090506.2+020700 | 163 | 347099 | 09:05:06.1 02:07:02.2 | 0.345 | 107.6 | 18.8 | N |
| J090030.0+012200 | 1160 | 301774 | 09:00:30.1 01:22:00.2 | 0.353 | 48.4 | 19.15 | Y |
| J085849.3+012742 | 2173 | 376723 | 08:58:49.4 01:27:41.0 | 0.355 | 46.2 | 18.71 | Y |
| J091435.3−000936 | 3132 | 575168 | 09:14:35.3 −00:09:35.6 | 0.359 | 40.6 | 19.02 | N |
| J090450.0−001200 | 3366 | 574555 | 09:04:50.1 −00:12:03.0 | 0.354 | 40.3 | 18.93 | Y |
| J090707.7+000003 | 4104 | 216048 | 09:07:07.9 00:00:02.1 | 0.350 | 46.2 | 19.38 | Y |
| J090845.3+025322 | 5323 | 518630 | 09:08:45.3 02:53:20.0 | 0.353 | 28.6 | 18.98 | N |
| J090658.6+020242 | 5347 | 382441 | 09:06:58.4 02:02:44.7 | 0.347 | 32.7 | 19.01 | Y |
| J090444.9+002042 | 5526 | 600545 | 09:04:44.9 00:20:48.2 | 0.342 | 31.2 | 19.23 | N |
| J090844.8−002119 | 6216 | 204249 | 09:08:44.8 −00:21:18.0 | 0.352 | 36.2 | 18.75 | N |
| J090402.3+010800 | 6418 | 372500 | 09:04:02.2 01:07:58.2 | 0.347 | 31.6 | 18.96 | Y |
| J090849.4+022557 | 6451 | 387660 | 09:08:49.5 02:25:56.9 | 0.353 | 33.7 | 19.08 | N |

Note. Positions and redshifts refer to the optical properties of the XID in Bourne et al. (2016). 250 μm flux is from the H-ATLAS DR1 release (Valiante et al. 2016). $r_p$ is the SDSS r-band petrosian magnitude from GAMA. SMG indicates whether a background high-redshift SMG is detected at >5σ in the Band 7 field.

### 2 SAMPLE AND DATA

The aim of the proposed ALMA observations was to map CO, dust, and [CI](3P1−3P0) in a sample of 250 μm selected galaxies to make a calibration of molecular gas mass based on three tracers. Full details of the project and results from the dust, CO, and [CI] imaging are presented in a companion paper (Dunne et al., submitted). The sample was selected from the Herschel–ATLAS (Eales et al. 2010) Science Demonstration Phase (SDP) equatorial field at R.A. 09h. H-ATLAS is the first unbiased survey of the dust content of local galaxies, covering 660 deg$^2$ and sensitive to the cold dust component which dominates the mass of dust in galaxies. It was the widest area extragalactic survey carried out with the Herschel Space Observatory (Pilbratt et al. 2010), imaging 600 deg$^2$ in five bands centred on 100, 160, 250, 350, and 500 μm, using the PACS (Poglitsch et al. 2010) and SPIRE instruments (Griffin et al. 2010). The Herschel observations consist of two scans in parallel mode reaching a 4σ point source sensitivity of 28 mJy beam$^{-1}$ at 250 μm. The angular resolution is approximately 9, 13, 18, 25, and 35 arcsec in each of the five bands. While the original sample for the proposal was selected from the SDP public release catalogue described in Rigby et al. (2011) to have $S_{250} > 5σ$ and a reliable optical identification with spectroscopic redshift from Smith et al. (2011), we update the Herschel photometry and optical parameters in this paper to those from the H-ATLAS DR1 release (Bourne et al. 2016; Valiante et al. 2016).

In order to fulfill the requirements of the ALMA Cycle 1 call where only Band 7 and Band 3 were available, all the sources had to be within 12 degrees of each other on the sky and had to be observed using no more than five tunings, resulting in a very limited redshift range around $z = 0.34–0.36$ that fulfilled these requirements. We selected all the H-ATLAS SDP sources within this redshift range, making this sample of 12 representative of sources from a blind 250 μm selected sample at $z \sim 0.3–0.4$. Details of the sample are given in Table 1.

The H-ATLAS DR1 photometry we use is given in Table 2, to which we add the ALMA 850 μm fluxes for the $z = 0.35$ sources which are taken from Dunne et al. (submitted). We use the SPIRE matched filter photometry from the DR1 release, as these are all point sources and this is the most likely estimate of their flux (Maddox & Dunne 2020). In the case of PACS, the LAMBDAR algorithm of Wright et al. (2016) produces, in our opinion, a more robust measure of the PACS fluxes and errors as instead of using
selected galaxies at the same redshift from the GAMA survey (Driver et al. 2011; Liske et al. 2015; Wright et al. 2016). Spectroscopic redshifts and UV–22 μm photometry are provided by the GAMA survey (Driver et al. 2011; Liske et al. 2015; Wright et al. 2016).

The sample has a narrow range of $L_{\text{IR}} = 1.2 \times 10^{11} - 6 \times 10^{11}$ $L_\odot$, making them far more ‘typical’ of galaxies at this redshift than previous very luminous IR samples (e.g. Combes et al. 2011). The stellar masses are in the range $M_\star = 4 \times 10^{10} - 3 \times 10^{11}$ M_\odot. Comparison of the 250 μm selected sources with other optically selected galaxies at the same redshift from the GAMA survey (Driver et al. 2016; Baldry et al. 2018) in Fig. 1 shows that the 250 μm selection picks out the leading edge of the optical cloud of galaxies, i.e. only the most massive or highly star forming galaxies at this redshift make it above the Herschel flux limit.

### 2.1 ALMA observations and data reduction

Observations in the 3 mm band were made in 2013 December during Cycle 1 with the ALMA Band 3 receiver tuned to 85 GHz. The total integration time for all 12 sources plus calibrations was 96 min giving $\sigma_{\text{cont}} = 40 \mu$Jy per synthesized beam of $\theta = 2.4 \times 1.8$ arcsec$^2$. The [CI($^{3}\Pi_{1}^{3}P_{0}$)] observations were split across Cycles 1 and 2 spanning a period from 2013 December–2015 January, and using four tunings of the Band 7 receiver in the range 362–367 GHz. The total integration time was 10.7 h giving $\sigma_{\text{cont}} = 65–90 \mu$Jy beam$^{-1}$ with $\theta = 1.03 \times 0.64$ arcsec$^2$. A list of the observations is presented in Table 3.

The 3 mm Band 3 data were reduced manually using the Common Astronomy Software Applications (CASA) v4.5 package (McMullin et al. 2007) with flux calibration from Mars and the phase/bandpass calibrator J0854+2006. The two measurement sets (MS), which were observed on the same day, were concatenated before imaging having been set to a common flux scale. We created spectral line cubes using TCLEAN in CASA in 100 km s$^{-1}$ channels, natural weighting was used in order to maximize signal to noise. We also imaged in spectral line mode, the three TDM windows which were used for the continuum at 3 mm. We did so in order to search for emission lines in the high redshift SMG discovered in our fields. The noise in these cubes was 0.4–0.5 mJy beam$^{-1}$, respectively.

The Band 7 observations were set up in four Scheduling Blocks (SBs) where the sources that could share a single tuning were grouped into a given SB. Due to some of these data being taken during Cycle 2, the newer CASA v4.7 was used for the reduction. Some of the MS were calibrated using the ALMA pipeline, while others were reduced manually, depending on how the data were delivered. All MS were checked and reprocessed allowing for tailoring of the calibration to the specific issues in this data set. For example, there are several atmospheric lines which are evident in the Band 7 data and so the pipeline calibration was modified to avoid flagging the system noise temperature ($T_{\text{sys}}$)$^{-1}$ response in some cases, and to

$$T_{\text{sys}}$$ is a representation of the noise from both receivers and the atmosphere and is used to calculate initial weightings of the visibility data. In spectral

### Table 2. FIR photometry for the $z = 0.35$ galaxies from Herschel-ATLAS DR1 and our ALMA measurements.

| Source | $S_{100}$ | $\sigma_{100}$ | $S_{160}$ | $\sigma_{160}$ | $S_{250}$ | $\sigma_{250}$ | $S_{350}$ | $\sigma_{350}$ | $S_{500}$ | $\sigma_{500}$ | $S_{850}$ | $\sigma_{850}$ |
|--------|-----------|---------------|-----------|---------------|-----------|---------------|-----------|---------------|-----------|---------------|-----------|---------------|
| 163    | 73.9      | 20.7          | 102.1     | 24.1          | 107.6     | 7.3           | 50.7      | 8.1           | 23.9      | 8.5           | 3.05      | 0.34         |
| 1160$^1$ | 49.8      | 17.5          | 57.1      | 19.7          | 48.4      | 7.2           | 32.4      | 8.1           | 21.6      | 8.7           | 0.54      | 0.12         |
| 2173$^1$ | 59.0$^M$  | 34.0          | 68.0$^M$  | 38.0          | 46.2      | 6.5           | 21.4      | 7.5           | 11.1      | 7.8           | 0.74      | 0.20         |
| 3132   | 64.3$^M$  | 26.5          | 65.1$^M$  | 20.0          | 40.6      | 6.4           | 23.6      | 7.4           | 13.1      | 7.8           | 0.95      | 0.29         |
| 3366$^1$ | 19.7      | 24.5          | 114       | 37.6          | 40.3      | 7.3           | 26.3      | 8.0           | 16.5      | 8.8           | 0.42      | 0.09         |
| 4101$^1$ | 77.9      | 17.6          | 53.3      | 26.4          | 46.2      | 7.2           | 28.3      | 8.1           | 12.1      | 8.8           | 0.92      | 0.24         |
| 5323   |           |               |           |               |           |               |           |               |           |               |           |               |
| 5347$^1$ | 33.0      | 41.2          | 68.0      | 17.7          | 32.7      | 7.5           | 29.8      | 8.2           | 17.2      | 8.7           | 1.84      | 0.35         |
| 5526   | 62.0$^M$  | 32.6          | 56.9$^M$  | 40.7          | 31.2      | 7.3           | 20.0      | 8.2           | 10.7      | 8.5           | 1.11      | 0.27         |
| 6216   | 35.0$^M$  | 36.6          | 34.0$^M$  | 40.7          | 36.2      | 7.3           | 19.9      | 8.1           | 3.8       | 8.8           | 1.49      | 0.25         |
| 6418$^1$ | 40.4$^M$  | 19.8          | 27.0$^M$  | 33.3          | 31.6      | 7.3           | 18.5      | 8.0           | 16.6      | 8.4           | 1.06      | 0.32         |
| 6451$^1$ | 69.4      | 41.7          | 59.5      | 47.8          | 33.7      | 7.3           | 29.7      | 8.2           | 19.5      | 8.6           | 0.88      | 0.19         |

*Note.* Fluxes are all in mJy. $^1$ indicates that there is evidence for contamination of these Herschel fluxes by high-z SMG in the beam. Before SED fitting, we subtract from these fluxes the estimated contamination from high-z SMG listed in Table 9. See Section 4 for details. $^M$ indicates a PACS flux re-measured from the DR1 maps.

### Figure 1. Star formation rate (SFR) versus stellar mass for the $z = 0.35$ sources with the best-fitting main sequence (solid) and ±0.3 dex intrinsic scatter (dashed lines) from Speagle et al. (2014). The coloured region represents the density of galaxies in the range $0.33 < z < 0.36$ with $\sigma_{\text{sSFR}} = -11.0$ and $\sigma_{\text{M}_\star} < 0.15$, $\sigma_{\text{SFR}} < 0.2$ from GAMA (Driver et al. 2016). This also shows the effect of the 250 μm selection at this redshift, where we sample the leading edge of the distribution in SFR–M_\star for the optical selection $r < 19.8$ from GAMA.
output the data set from the pipeline after the generation of the water vapour radiometer (WVR) and \(T_{\text{sys}}\) calibration tables. The data were then manually processed from that stage so that the atmospheric lines could be flagged in the bandpass calibrator and the bandpass solutions interpolated in these regions. Additional manual flagging was also applied where required.

During imaging, it was obvious from the dirty images that there were point sources in the fields of at least half of the targets, which were not associated with the \(z = 0.35\) system. They were very obvious as they were usually much higher SNR than the target source itself. We did not run any source extraction algorithms, but merely noted when a bright point source was present in the imaging (as it needed to be cleaned) and later on went back to analyse these serendipitous detections. To check the robustness of these sources, we made two analyses. First, we noted the flux and SNR of each SMG in all of the different execution blocks (EB) in which they were observed. Four of the SMG were observed in four execution blocks, three on the same night and another taken almost a year earlier. The other three SMG were all those detected with SNR \(> 3\) in the image plane for sources which are smaller than the synthesized beam. Fitting in the \((u,v)\) plane is more direct and avoids the uncertainties associated with the non-linear process of deconvolution in the imaging. The fluxes and sizes are reported in Table 6, the first row for each source lists the parameters from the \((u,v)\) fitting while the second row lists the peak flux reported by IMFIT (equivalent to a point source flux).

For the \((u,v)\) fitting, we averaged the data across each spectral window and in intervals of 30 s, both of these do not lead to significant band-width or time smearing for this ALMA band. We then fixed the phase centre to be the position of the SMG and fitted with a 2D Gaussian where the flux \(S_{\text{ph}}\), position, major axis size \(\theta_{\text{maj}}\), and position angle (pa) were free parameters. The sixth parameter, the axial ratio \(b/a\), was found to be unconstrained by fitting, tending to an axial ratio approaching zero, usually aligned with the pa of the beam. This tendency produces a bias in the values for \(S_{\text{ph}}\) and \(\theta_{\text{maj}}\), both of them being maximized. Since an axial ratio approaching zero is not physical, we have used a constrained fit as described in Appendix A.

2.2 Flux and size measurements

We measured the fluxes of the source in two ways, first by fitting a Gaussian and taking the peak flux from the CASA task IMFIT, and secondly, by fitting a Gaussian in the \((u,v)\) plane using UVMODELFIT (Martí-Vidal et al. 2014). We used both methods as a check for systematics, and also because very little size information can be derived in the image plane for sources which are smaller than the synthesized beam. In this way, we avoid the uncertainties associated with the non-linear process of deconvolution in the imaging. The fluxes and sizes are reported in Table 6, the first row for each source lists the parameters from the \((u,v)\) fitting while the second row lists the peak flux reported by IMFIT (equivalent to a point source flux).

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The major axis source sizes fitted in this way range from 0.1 to 0.6 arcsec, and the average value of the circularized size is \(\theta = 0.36\) arcsec, which translates to \(R_e \sim 2\) kpc for \(z = 1–3\). This value is comparable to other studies of SMG in which the sources were much better resolved, and so this gives a measure of confidence in our fluxes and sizes (Simpson et al. 2015; Hodge et al. 2016; Oteo et al. 2016; Rujopakarn et al. 2016; Fujimoto et al. 2017; Tadaki et al. 2017; Lang et al. 2019). The limit for reliable size determination in interferometric observations is given by Martí-Vidal, Pérez-Torres & Lobanov (2012), and using their equation (7) with \(\beta = 0.75\) and \(\lambda_c = 3.84\), the \(2\sigma\) limit to the minimum size which could be reliably measured for our sources is listed in Table 6. Two of the sources have fit results which are comparable or slightly smaller than this limit and so for these we quote the \(2\sigma\) upper limit to their sizes (SDP.5347, SDP.6418). Fig. 2 shows the azimuthally binned \((u,v)\) data, together with the model representing the best fit for the median likelihood axial ratio, \(a/b = 0.75\).

There is a small difference between the peak flux derived from the fit to the imaging and the 2D fit to the \((u,v)\) data described above (where the size is a free parameter), such that the integrated fluxes from the fits with finite size are higher than the point source fluxes. This is expected, a point source flux estimate will always underestimate the flux of a source with a finite size, the degree of underestimation being dependent on the ratio of the source area compared to the beam area. To be certain that this distinction (which

| SB name | \(v_{\text{obs}}\) (GHz) | Date       | MS  | \(N_{\text{ant}}\) | \(t_{\text{int}}\) (min) | p.w.v (mm) | Phase Cal. | Flux Cal. | B.P. | \(\sigma_{\text{cont}}\) (\(\mu Jy\)) |
|----------|-----------------|-----------|-----|-----------------|-----------------|------------|------------|----------|-----|-------------------|
| LowV     | 365.2           | 14.12.13  | X1644 | 26              | 50.2            | 0.84       | J0854 + 20 | Pallas   | J1058 + 01 | 90 | 0.86–1.2          |
|          | 26.12.14        | X2543     | 40   | 33.3            | 0.84            | J0909 + 01 | Ganymede   | J0825 + 03 | ..  | ..                |
| HighV    | 363.5           | 21.2.14   | X3e5 | 28              | 35.3            | 0.64       | J0914 + 02 | Ganymede   | J0825 + 03 | 65 | 0.84–1.1          |
|          | 2.1.15           | X1e75     | 39   | 34.2            | 0.69            | J0909 + 01 | Callisto   | J0825 + 03 | ..  | ..                |
|          | 2.1.15           | X2365     | 39   | 15.4            | 0.82            | J0909 + 01 | Ganymede   | J0825 + 03 | ..  | ..                |
|          | 2.1.15           | X2606     | 39   | 34.2            | 0.91            | J0909 + 01 | Ganymede   | J0909 + 01 | ..  | ..                |

\(\sigma_{\text{cont}}\) is the average rms in \(\mu Jy\) beam\(^{-1}\) for the continuum.

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Note. \(\sigma_{\text{cont}}\) is the average rms in \(\mu Jy\) beam\(^{-1}\) for the continuum.
Table 4. Robustness check of detection of SMG in the individual data sets.

| EB      | Typical rms (μJy beam$^{-1}$) | Signal-to-noise ratio of the SMG in each individual EB. |
|---------|-------------------------------|--------------------------------------------------------|
|         |                               | 1160.s1 | 1160.s2 | 2173 | 3366 | 4104 | 5437 | 6418 |
| X3e5    | 136                           | 5.7     | 3.4     | 3.8  | 5.5  | –    | –    | –    |
| X1e75   | 100                           | 7.9     | 8.4     | 5.3  | 4.6  | –    | –    | –    |
| X2365   | 171                           | 3.5     | 4.6     | 3.6  | 3.9  | –    | –    | –    |
| X2606   | 170                           | 4.8     | 3.1     | 3.8  | 5.5  | –    | –    | –    |
| X1644   | 163                           | –       | –       | –    | –    | 3.7  | 3.5  | 12.8 |
| X2543   | 103                           | –       | –       | –    | –    | 5.0  | 7.2  | 15.2 |

Note. This table records the SNR of each SMG in all of the individual execution blocks. In every case, there is a positive source at the same position in each EB. Sources brighter than 4σ were cleaned, there is no significant change in properties with or without cleaning applied (except for the brightest source 6418, which is bright enough to self calibrate).

Table 5. Results of inverting the images for the SMG fields.

| Field   | Number of peaks in given signal-to-noise range |
|---------|-----------------------------------------------|
|         | (< –5) | (–5, –4) | (4,5) | (5,6) | (>6) |
| 1160    | 0      | 1        | 1$^*$ | 0     | 2    |
| 2173K   | 0      | 0        | 1     | 0     | 1    |
| 3366K   | 0      | 1        | 1     | 0     | 1    |
| 4104K   | 0      | 0        | 1$^*$ | 1     | 0    |
| 5347K   | 0      | 0        | 0     | 0     | 1    |
| 6418    | 0      | 0        | 0     | 0     | 1    |

Note. Number of negative peaks more significant than −4σ compared to the positive peaks as a simple test of source robustness. There are no negative peaks at < −5σ while there are seven peaks at > +5σ. A $^*$ symbol at the field name indicates that the SMG has a K-band counterpart. A $^*$ symbol indicates that this positive peak is the target low-z galaxy.

for the most part is not highly significant, the most significant being SDP.4104.s1 at 2.6σ. A K symbol at the field name indicates that the SMG has a K-band counterpart. A $^*$ symbol indicates that this positive peak is the target low-z galaxy.

3 AN OVERDENSITY OF HIGH REDSHIFT SMG AROUND MASSIVE GALAXIES AT z = 0.35

Half of the fields observed contained one or more serendipitously detected high redshift SMG. In total seven SMG are confidently detected at $S_{850} > 5σ$ in six fields. The details of these SMG are given in Table 6 and images are shown in Fig. 3. We give detailed notes on each source in Appendix B.

We looked for counterparts to these SMG in VIKING K-band imaging (Edge et al. 2013; Driver et al. 2016), which is the deepest ancillary data set in this region, and find K-band counterparts to four out of seven SMG. Counterparts or upper limits to the K-band magnitudes are noted in Table 6 and the K-band images are shown also in Fig. 3.

3.1 Overdensity calculation

In order to estimate 850 μm number counts from this sample, we must first sum the area observed in which a given source could have been detected with an SNR $> 5σ$.

The sensitivity of our ALMA pointings is not uniform due to the tapering effect of the primary beam. We created a noise-map for each of the 12 fields to capture this radially varying noise level by multiplying the primary beam attenuation image by the rms noise measured in a source-free region of the flux image before primary beam correction. This gives us a map of the average noise as a function of radius for each field. For the 12 noise-maps (one for each of the 12 target fields), we sum the area over which we could have detected each source at its peak measured flux at a significance level of five times the local noise. The surface density of a source of a given flux is then simply the inverse of this area.

There are currently only two published measures of the faint number counts at 850 μm using ALMA, those from Oteo et al. (2016) (hereafter O16) who used the ALMA calibrator data set to produce a direct and unbiased measurement of the 850 μm counts with ALMA down to sub-mJy levels, and more recently those from Bethermin et al. (2020) (hereafter B20) who present serendipitous 850 μm sources detected in fields targeted at $z > 4$ [CII] emitters. Both of these analyses were performed in comparable ways to ours, with an SNR $≥ 5$ selection criteria and measurement of the source fluxes using integrated 2D Gaussian fitting (although both of these works used image plane rather than ($u$, $v$) fitting).

With such small numbers, we cannot hope to make an accurate measure of the counts since our uncertainties are always going to be dominated by counting statistics. Our aim in this paper is to determine with some confidence level whether we are seeing a statistical overdensity of SMG in these fields containing massive $z = 0.35$ galaxies. In order to do this, we will compare our results to those of O16 and B20, exploring the impact of different criteria for the flux measurement, and the magnitude of completeness corrections. In each comparison, we utilize the results of simulations by O16 and B20, who provide completeness estimates for samples similarly selected with SNR $≥ 5$.

To begin with, we provide short summary of the methods used by each of the comparison counts analyses and highlight any points of difference.

O16 measure fluxes by fitting 2D Gaussians to the image plane and using the integrated flux, although sources are detected with an

$^2$The ALMA images have not been corrected for the variable attenuation of the primary beam. A source nearer to the edge of the map will have a higher flux at the same signal-to-noise contour level compared to a source in the centre. This is due to the fact that the primary beam attenuation increases the noise as a function of radius from the pointing centre.

$^3$Given that our least significant source is actually 6σ, going down to 5σ provides a more generous area and therefore lower density estimate than if we had stated a cut off at 6σ.
measurements are explicitly mentioned in B20, we have used their
the peak pixel flux is significantly greater than unity. While no size
imaging, based on their finding that the ratio of the integrated flux to
the sources are marginally resolved by their 
\[ \sim \]
which have measured the sizes of SMG, Bethermin et al. infer that
Despite having a larger beam size compared to O16 (and other studies
in the image plane, having detected the source based on a peak
visibilities and recovered using their normal procedure in a uniform
simulated sources are all point-like while the real sources would be
in the B20 simulations, sources are injected directly into the image
plane rather than into the (u, v) plane using VMOODELFFT, where the size fitted is
SNR = 6 compared to those produced in O16 (80 per cent for O16, 25–30 per cent for a source with the average
size of 0.72 arcsec implied by Fig. 4 in B20). Thus, for a given set of
sources, detected and measured in identical ways the Bethermin et al.
method would produce counts a factor \( \sim 3 \) larger than using the Oteo et al.
method, solely due to the size dependence of the completeness
and the interpretation of the peak/integrated flux ratio as a size measurement by Bethermin et al. (2020).\footnote{\textsuperscript{4}}
Having contrasted the methods and data sets used we now contrast the number counts quoted by each survey. O16 use a fitting formula which describes the counts all the way from 0.4 mJy to the bright-end measured with ALMA by Simpson et al. (2015).
\[ N_{580}(> S) = N_0 \left[ \left( \frac{S}{S_0} \right)^\alpha + \left( \frac{S}{S_0} \right)^\beta \right]^{-1}, \]
where \( N_0 = 46.4 \text{ deg}^{-2}, S_0 = 8.4 \text{ mJy}, \alpha = 1.9, \) and \( \beta = 10.5. \) B20 do not fit a function to their counts but present the cumulative counts in bins, which we logarithmically interpolate to the flux values of interest to us.
The counts for the two analyses are presented in Table 7, where we are listing the ‘robust \( z < 4 \)’ counts from B20 to ensure we are not including any overdensity associated with the target sources. The B20 counts are higher by a factor 1.7–2.5 compared to those of O16.\footnote{\textsuperscript{5}}
We must acknowledge two factors in the way the counts have been obtained which may make the B20 counts tend to be higher than those of O16. First, the fields used to derive the B20 counts are targeted at

\begin{table}
\centering
\caption{Serenopitucus robust SMG found in the fields surrounding \( z = 0.35 \) H-ATLAS sources.}
\begin{tabular}{lcccccccc}
\hline
SMG & R.A. & Dec. & \( S_{850} \) & SNR & decon. size & \( \theta_{\text{min}} \) & r & K\textsubscript{AB} \\
& & & (mJy) & & (arcsec) & (arcsec) & & \\
\hline
1160.s1 & 09:00:30.40 & -01:22:02.90 & 1.06 \pm 0.08 & 11.4 & 0.4 \pm 0.09 \times 0.3 \pm 0.08 & 0.20 & 5.0 & 0.82 \> 21.32 \\
1160.s2 & 09:00:30.17 & -01:22:12.44 & 4.05 \pm 0.40 & 11.1 & 0.34 \pm 0.1 \times 0.26 \pm 0.09 & 0.21 & 12.5 & 0.20 \> 21.32 \\
2173.s1 & 08:58:49.26 & +01:27:48.3 & 1.05 \pm 0.11 & 6.3 & 0.44 \pm 0.12 \times 0.33 \pm 0.10 & 0.28 & 7.5 & 0.59 21.45 \pm 0.03 \\
3363.s1 & 09:04:50.20 & -00:12:10.0 & 0.82 \pm 0.073 & 11.0 & 0.39 \pm 0.10 \times 0.29 \pm 0.09 & 0.21 & 3.4 & 0.91 19.02 \pm 0.03 \\
4104.s1 & 09:07:07.47 & -00:00:06.9 & 0.74 \pm 0.067 & 6.0 & 0.6 \pm 0.19 \times 0.45 \pm 0.10 & 0.29 & 7.2 & 0.58 20.65 \pm 0.12 \\
5347.s1 & 09:09:58.65 & +02:02:51.9 & 1.30 \pm 0.21 & 7.4 & 0.25 \pm 0.22 \times 0.19 \pm 0.12 & < 0.26 & 8.0 & 0.52 21.55 \pm 0.31 \\
6418.s1 & 09:04:02.38 & +01:07:53.4 & 2.56 \pm 0.09 & 23.7 & 0.106 \pm 0.095 \times 0.08 \pm 0.065 & < 0.15 & 6.0 & 0.75 \> 21.32 \\
\hline
\end{tabular}
\textit{Note.} Name of SMG, R.A., and Dec., \( S_{850} \): 850 \( \mu \)m flux from two methods. First row from fitting in the (u, v) plane using VMOODELFFT, where the size fitted is also quoted. Second row is a minimum flux estimate, using the peak of a Gaussian fitted to the image with IMFF. SNR: signal-to-noise ratio from the peak pixel and rms map noise. \( \theta_{\text{decon}} \): Deconvolved size from the (u, v) fitting (see the text for details). \( \theta_{\text{min}} \) is the minimum reliable size which can be measured given the SNR of these sources using the formalism of Martí-Vidal et al. (2012). Where the fitted size is comparable to or smaller than this size, we quote the 2\sigma size limit in this column. r distance of the SMG to the centre of the target \( z = 0.35 \) galaxy in arcseconds. P.B.: the primary beam correction which has been applied to these fluxes. K\textsubscript{AB}: \( K \)-band magnitude (AB) or 3\sigma limit at the position of the SMG using VIKING data.\footnote{\textsuperscript{1}} flux measured in a 2 arcsec aperture on VIKING image created by Driver et al. (2016).\footnote{\textsuperscript{2}} flux measured on VIKING image using SEXTRACTOR to deblend the red object from the foreground and using MAG_AUTO.
\end{table}

initial peak pixel flux requirement SNR \( \geq 5 \). The beam sizes are 0.4 \( \times \) 0.3 arcsec\(^{2}\) for eight sources, and 1 \( \times \) 0.6 arcsec\(^{2}\) for three sources. Their simulations consist of point sources injected into the visibilities and recovered using their normal procedure in a uniform manner. These simulations demonstrate that completeness reaches \( \sim 80 \) per cent at SNR = 6 for catalogues with a 5\sigma detection threshold (Oteo et al. 2016). This is likely to be the best case scenario as the simulated sources are all point-like while the real sources would be expected to have finite sizes (particularly in the cases with smaller synthesized beams).

B20 also measure their fluxes using integrated 2D Gaussian fitting in the image plane, having detected the source based on a peak pixel SNR \( \geq 5 \). The beam sizes are typically 1.2 \( \times \) 0.8 arcsec\(^{2}\). Despite having a larger beam size compared to O16 (and other studies which have measured the sizes of SMG), Bethermin et al. infer that the sources are marginally resolved by their \( \sim 1 \) arcsec resolution imaging, based on their finding that the ratio of the integrated flux to the peak pixel flux is significantly greater than unity. While no size measurements are explicitly mentioned in B20, we have used their equation (4) and Fig. 4 which relate the peak/integrated flux ratio to \( \Omega_{\text{source}} / \Omega_{\text{beam}} \), to estimate the average implied deconvolved size of their sources as \( \sim 0.72 \) arcsec. The beam size for our data set is similar to B20, and yet our (u, v) plane analysis indicates that our sources have a size \( < 0.52 \) arcsec, with a mean of 0.31 arcsec, comparable to the average size measured for SMG in the literature (\( \sim 0.3 \) arcsec; Lang et al. 2019 and references within). The upper range of the reported sizes in the literature is \( R_{\theta} \sim 4.5 \) kpc (Rujopakarn et al. 2016), which translates to FWHM\( \sim 0.68 \) arcsec for redshifts greater than unity. It is noteworthy that the average size of \( \sim 0.72 \) arcsec implied by the B20 analysis of the peak-to-integrated flux ratio is larger than the upper end of the range found in all of the rest of the SMG literature. This has implications for our comparison of number counts, because B20 perform their simulations of completeness including size as a variable, finding that the larger sources have much lower completeness at a given detection signal-noise ratio. In the B20 simulations, sources are injected directly into the image plane rather than into the (u, v) visibilities as in O16. As a result, the completeness corrections derived by B20 are very different at the detection threshold SNR = 6 compared to those produced in O16 (80 per cent for O16, 25–30 per cent for a source with the average size of 0.72 arcsec implied by Fig. 4 in B20). Thus, for a given set of sources, detected and measured in identical ways the Bethermin et al. method would produce counts a factor \( \sim 3 \) larger than using the Oteo et al. method, solely due to the size dependence of the completeness correction, and the interpretation of the peak/integrated flux ratio as a size measurement by Bethermin et al. (2020).\footnote{\textsuperscript{4}}

\begin{figure}
\centering
\includegraphics[width=\textwidth]{figure.png}
\caption{Example figure.}
\end{figure}

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Figure 2. The binned $u,v$ data with Gaussian fits from UVMODELFIT overplotted for the seven SMG. Details of the fit parameters are in Table 4. In all cases the data were averaged in frequency to one point per spectral window and in time by 30 s before fitting. Points are averaged in radial bins of $u-v$ distance using the weights from CASA. Error bars on points are estimated from the scatter of the data points within each bin (this is comparable but slightly larger than using the inverse square-root of the sum of the weights).
Figure 3. Panels for each field containing SMG, showing from left to right: Left-hand panel: $K$-band image from VIKING (Edge et al. 2013) with ALMA 850 $\mu$m contours overlaid in red, starting at 4$\sigma$. The stretch is made to highlight any faint $K$-band emission from the position of the SMG. Centre: ALMA 850 $\mu$m image zoomed in and centred on the SMG(s) with contours starting at 4$\sigma$. Negative contours are shown starting at $-4\sigma$ as black dashed lines. Right-hand panel: For the four fields with $K$-band emission at the SMG position we show colour composites from VST Kilo Degree Survey (de Jong et al. 2017) and VIKING which highlight the very red colours of those sources. For SDP.1160 and SDP.6418, there is no sign of any $K$-band emission down to the VIKING 3$\sigma$ limit of $K_{AB}=21.3$.

Figure 4. The cross-correlation signal for background SMG and foreground structure in the range $0.2<z<0.8$ from SDSS and GAMA. The grey points are the results of the statistical cross-correlation using H-ATLAS sources with estimated FIR photo-$z>1$ from GN17. The red points are the SMG found in the fields of our $z=0.35$ targets in two radial bins. The solid blue line is for an NFW halo with $M_{200c}=7 \times 10^{13} M_{\odot}$ and concentration parameter $C=5.5$. The dashed lines represent the model with a variation of $\pm 30$ per cent in $C$, while the translucent solid lines show a variation of $\pm 30$ per cent in halo mass.

Due to this uncertainty, we proceed to calculate our overdensities with three different assumptions about the completeness correction:

(i) No completeness correction applied – gives a minimum estimate of the counts for our fields.

(ii) Completeness correction following O16 simulations, meaning our two sources with SNR $\sim 6$ (SDP.2173, SDP.4104) have corrections of 80 per cent applied to them.

(iii) Completeness correction following B20 size-dependent simulations, adopting the sizes measured for our sources using the $n$, high-redshift galaxies with high star formation rates. They are therefore biased sightlines as galaxies are clustered, thus an extra signal at the same redshift might be expected. For this reason, we compare to the robust $z<4$ counts from B20 which will have removed any contamination from clustered sources at the same redshift as the targets. There is, however, another more subtle bias which may be present, which is in fact the topic of this paper. Magnification lensing bias means that the pre-selection of fields containing bright, high redshift objects increases the probability of sight-lines containing more large-scale structure; which weakly lenses the high redshift sources making them appear slightly brighter, and hence more likely to be selected as targets. Dusty galaxies present in any foreground structures could create a bias to higher number counts. Secondly, as mentioned earlier, the completeness corrections adopted by each study are very different, with the size-dependent completeness correction of B20 leading to much higher corrections on average for their sources compared to the point source estimates of O16.
v fitting (see Table 6). This gives a completeness for SDP.2173 of 80 per cent (as it is compact) but for SDP.4104, the largest source, completeness is only 35 per cent.

In Table 7 we present the counts we measure with each of the three completeness scenarios. We list the overdensity of sources in our survey relative to both the predicted number counts from Oteo et al. (2016), and relative to the robust \((z < 4)\) sample from B20. The minimum overdensity we find when we apply no completeness correction to our counts at \(S_{\text{50}} > 0.8\), 1.3 mJy, is 6.6–7.5 for O16 and 3–4 for B20. Furthermore, in contrast to the other studies, we have not excluded the area in the centre of the map which is covered by the target optical galaxy, which makes our surface density estimates lower limits.

Making a fairer comparison between our data and the literature, if we compare our counts using the O16 completeness correction to the O16 counts, we find an overdensity of a factor 7–8. If we compare our counts using the B20 completeness correction to the B20 counts, we find overdensity factors of 5–5.5.

We have estimated the 1-σ uncertainties on our overdensity measurements using the Bayesian approach described by Kraft, Burrows & Nousek (1991). We used the same approach to estimate the probability that we could find the observed number of sources in our fields given the null hypothesis that there is no overdensity compared to the background counts. Using the O16 counts, the resulting probability rules out the null hypothesis at the 4-σ level; using the B20 counts the null hypothesis is ruled out at 3.6-σ. So, even though our overdensity estimates have large uncertainties, we are confident that there is a significant overdensity in our fields.

We next consider a possible physical explanation for this excess of SMG.

### 3.2 Lensing magnification bias

Cross-correlations between foreground structure traced by SDSS galaxies and background galaxies detected by Herschel have been detected with high significance (González-Nuevo et al. 2014, 2017). Anomalies in the positional offset distribution between Herschel-ATLAS sources with high-redshift submillimetre colours and foreground optical galaxies are also seen (Bourne et al. 2014). These findings both imply that there is significant magnification of the background SMG population by large-scale structure in the foreground. The recent work by González-Nuevo et al. (2017) (hereafter GN17) shows that lensing from the foreground halo will produce an overdensity of SMG relative to the unlensed background within \(r < 20\) arcsec of haloes with \(\log M_\bullet / M_\odot > 13.5\). The magnitude of the overdensity will correlate with the distance of the SMG from the projected centre of the halo mass distribution.

We have computed the relative overdensity of SMG as a function of radius from the centre (assuming that the target \(z = 0.35\) galaxy is the centre of its halo). Fig. 4 shows our estimated cross-correlation (red dots) compared to the cross-correlation measurements obtained by GN17 (grey squares), who studied the magnification bias due to luminous red galaxies with \(0.2 < z < 0.8\) from GAMA (Baldry et al. 2018) which act as lenses on the high redshift (\(z > 1.2\)) SMG detected by H-ATLAS. There is a good agreement between both sets of measurements. To derive physical information on the typical halo that can produce such magnification bias, we perform a similar analysis to that described in Bonavera et al. (2019). By neglecting the shear effect in the magnification bias, Bonavera et al. exploit the direct relationship between the cross-correlation function and the halo convergence: \(\kappa(\theta) = 1 - (\varpi(\theta) + 1) \pi^2\), where \(\beta > 3\) is the slope of the integrated source counts of the background SMG sample. As is common in previous works analysing the magnification bias, we model a Navarro Frenk and White (NFW: Navarro, Frenk & White 1997) mass density profile with the mass, \(M_{200c}\), and concentration, \(C\). The data do not allow a direct constraint with the current statistics, but Fig. 4 shows that they are consistent with typical values of \(M_{200c} = 7 \times 10^{13} M_\odot\) and \(C = 5.5\) (blue solid line). Varying each parameter by ±30 percent produces the dashed lines (C) and the pale blue solid lines (\(M_{200c}\)). There is intrinsic degeneracy between mass and concentration in the fitting, and to provide direct constraints will require a larger sample which could be split over more radial bins.

The values which are representative of the cross-correlation are in good agreement with the \(M_{200c}\) versus \(C\) relationships from Child et al. (2018) and Dutton & Macciò (2014). The magnifications expected at \(r = 3–12\) arcsec for haloes this massive are of the order \(\mu = 1.5–3\) (González-Nuevo et al. 2014) which is enough to make a substantial overdensity of SMG visible due to the steep number counts in the sub-mm waveband. This halo mass corresponds to \(M_\bullet \sim 1 – 3 \times 10^{11} M_\odot\) using the relationships for \(M_{200c} – M_\bullet\) from both Moster et al. (2010) and Behroozi, Wechsler & Conroy (2013). We might expect to find a small group of galaxies consisting of a bright, massive central galaxy with a few additional dwarf satellites of much lower mass.

The six SMG fields have central galaxies with \(M_\bullet = 6.5 \times 10^{10} – 1.6 \times 10^{11} M_\odot\); four of the six central galaxies are interacting with smaller satellites (evidence for this is the optical morphology and kinematics of CO and [CI], see Dunne et al. submitted for details), and a fifth (SDP.1160) is a member of a GAMA spectroscopic group with another \(r < 19.8\) galaxy lying outside the ALMA B7 field of view. The only galaxy for which we have no

### Table 7. The number counts estimated from our data compared to other ALMA counts at 850 μm.

| \(S_{\text{50}}\) (mJy) | \(n\) | Reference counts | \(N_{\text{obs}}(> S)\) (deg\(^{-1}\)) | \(N_{\text{sd}}(> S)\) (deg\(^{-1}\)) | \(N_{\text{bg}}(> S)\) (deg\(^{-1}\)) | Overdensity observed | Overdensity corrected | \(P(\text{null})_{\text{obs}}\) (σ) | \(P(\text{null})_{\text{cor}}\) (σ) |
|-----------------|------|------------------|-----------------|-----------------|-----------------|---------------------|---------------------|--------------------------|--------------------------|
| 0.82            | 7    | O16              | 25 735          | 28 089          | 3861            | 6.7±0.9             | 7.3±0.4             | 3.9                      | 4.0                      |
| 1.3             | 4    | –                | 12 109          | 13 266          | 1609            | 7.5±0.5             | 8.2±0.9             | 3.1                      | 3.2                      |
| 0.82            | 7    | B20              | 25 735          | 35 529          | 6431            | 4.0±0.1             | 5.5±0.4             | 3.1                      | 3.6                      |
| 1.3             | 4    | –                | 12 109          | 20 707          | 4033            | 3.0±0.1             | 5.1±0.3             | 2.1                      | 2.7                      |

Note. Estimated counts in bins of 850 μm flux. \(n\) is the number of sources per bin, \(N_{\text{obs}}(> S)\) is the surface density we measure not corrected for completeness, \(N_{\text{sd}}(> S)\) accounts for the completeness correction using the same method as the background counts being compared to, \(N_{\text{bg}}(> S)\) are the background cumulative counts from Oteo et al. (2016) (O16) and Bethermin et al. (2020) (B20), respectively. These are corrected for completeness. The overdensity columns are the relative overdensity in our fields (both uncorrected and corrected for completeness) compared to the literature ‘blank-field’ measures including 1σ errors derived from the approach of Kraft et al. (1991). \(P(\text{null})\) is the significance at which the null hypothesis is rejected (that the number of sources we see is a random realization of the number counts given by the literature reference).
spectroscopic evidence for a close neighbour is SDP.2173, although there are three dwarfs in the GAMA group catalogue (Cavuoti et al. 2015; de Jong et al. 2017; Wright et al. 2019) which have $z_{\text{ph}} = 0.37–0.38$ located 40–90 kpc in projection and could very plausibly be in the same halo. SDP.2173 also has the brightest $r$-band magnitude of any of the sources we observed, $R_{\text{tot}} = -21.70$. All four of the interacting systems in our sample of 12 have an SMG in the field. The GAMA survey is highly spectroscopically complete for interacting systems in our sample of 12 have an SMG in the field.

The GAMA survey is highly spectroscopically complete for the target galaxy in arcsec. The environments and optical properties of the SMG field target galaxies are listed in Table 8.

4 BOOSTING OF THE H-ATLAS FLUXES BY SMG IN THE BEAM

Lensing by the halo of the massive $z = 0.35$ system increases the probability of finding a high redshift SMG within the same Herschel beam as the target low redshift source. This is a proverbial can of worms for modelling statistical properties of sub-mm surveys, e.g. source counts, sub-mm colour distributions, and SED modelling. Flux boosting from the SMG will affect all SPIRE fluxes, but those at longer wavelengths disproportionately so for two reasons. First, the Herschel beam is larger at longer wavelengths, thus a contaminant at distance $d$ will have a higher beam profile weighting at longer wavelengths. Secondly, the sub-mm colour of the high redshift SMG will be redder (relatively brighter at 500 μm) compared to the target source, as the observed frame samples closer to the peak of the SED at high redshift. The percentage contamination to the 500 μm flux from the high-z SMG is thus larger than that at 250 μm.

To estimate the contamination of the H-ATLAS fluxes for this sample at $z = 0.35$, we take the ALMA 850 μm flux measured for each SMG ($S_{\text{SMG}}$) and calculate the SPIRE fluxes the SMG should contribute to the H-ATLAS fluxes. For the remaining possible redshifts we calculate $S_{\lambda}^C$, the contribution of the SMG to the Herschel $\lambda$ μm fluxes of the $z = 0.35$ galaxy, by weighting the predicted SMG flux in each SPIRE band by the beam attenuation at the location of the $z = 0.35$ galaxy relative to the position of the SMG:

$$ S_{\lambda}^C = S_{\text{SMG}} \left( \frac{850 \mu m}{\lambda} \right)^{4+\beta} \frac{1}{\beta + 4} \frac{\lambda e^{(4+\beta)z/d_{\text{arcsec}}}}{\lambda e^{4z/d_{\text{arcsec}}}} - 1 e^{-d_\text{arcsec}^2/0.366^2} $$

Here $\lambda$ refers to the SPIRE wavelength of interest in μm, $\beta$ is the relevant beam size for SPIRE (18, 25, and 35 arcsec for the 250, 350, and 500 μm bands), $S_{\text{SMG}}$ is the 850 μm ALMA flux of the SMG and $z$ is the redshift chosen for the prediction. The dust SED parameters we use are $T_d = 38 K$ and $\beta = 1.8$, which are plausible values for SMG (Chapman et al. 2005; da Cunha et al. 2015; Stach et al. 2019), and $d$ is the separation between the SMG and the centre of the target galaxy in arcsec.

To determine the most likely contamination values, we step through in redshift from 1.5 to 5 in steps of $\Delta z = 0.5$, calculating the estimated contamination signal at each redshift. We adjust the H-ATLAS catalogue fluxes for the low redshift targets (Table 2) by these contamination values and then fit the SED from UV–850 μm using MAGPHYS (see Section 4.2). We choose the redshift ($z_{\text{SED}}$) at which the correction produces the lowest overall $\chi^2$ for the SED fit; $z_{\text{SED}}$ and contamination values are listed in Table 9.

The redshift and $T_d$ are roughly degenerate in this process but we are not attempting to constrain either; merely we wish to retrieve FIR colours which
fits when the SMG is assumed to be at $z = 1.5$–2 while those without $K$-band counterparts have better fits when the SMG is assumed to have $z > 3$.

The boosting effect will also mean that a low redshift sub-mm source is more likely to be above the detection threshold in a flux-limited survey if its halo is acting as a lens for an SMG with small projected separation. In order to see what effect the best estimate of our boosting has on our initial sample selection, we subtract the $250\mu m$ contamination in Table 9 from the flux reported in the H-ATLAS SDP catalogue from Rigby et al. (2011). We then determine how many of the sources would still have been in the catalogue at $S_{250}/\sigma_{250} \geq 5$ had there been no SMG. There is clearly a lot of uncertainty in this rough estimate because a wide range of contamination $250\mu m$ fluxes still produce acceptable fits to both the Herschel maps and the SED fits. The two brightest sources with SMG in the field (SDP.1160 and SDP.2173) remain at $S_{250} > 5\sigma_{SDP}$ for any reasonable SMG contamination estimate. Of the other four, there are possible redshift ranges where the contamination would still allow them to remain in the sample (e.g. $z > 2.5$ for SDP.3366 and SDP.4104, $z > 3$ for SDP.5347 and $z > 5$ for SDP.6418).

Depending on the redshift of the SMG, it is entirely possible that all six source would remain in the SDP sample even without the presence of the SMG, for the best estimate of contamination in Table 9 4/6 would remain in the sample and in the worst case, pushing the contamination to the highest permitted values only 2/6 would remain.

The possibility that the high fraction of ‘lensing’ systems in our $250\mu m$ catalogue is higher than it should be due to the effect of the boosting does not negate the magnification lensing bias as an explanation for this effect, however it would need to be accounted for in the modelling to derive more accurate parameters. This is beyond the scope of this study, and much larger samples which could be selected in flux bins to mitigate this uncertainty would be required to exploit this further.

### 4.1 How much boosting is there for flux limited surveys with Herschel?

The sample of 12 galaxies at $z = 0.35$ targeted by ALMA is a blind sample of $250\mu m$ selected sources from H-ATLAS, and while small, it is an unbiased set of sources from that survey. The implications of so much boosting in the long wavelength H-ATLAS photometry could be profound. Taking the results from Tables 2 and 9, we find that the average $350 (500)\mu m$ boost for the fields with SMG is 1.44 (1.75). If we assume the other fields have no contamination at all then we arrive at a global average boost factor of 1.26 (1.44) at $350 (500)\mu m$. This is significantly higher than that estimated from the simulations for the H-ATLAS data release (DR1) by Valiante et al. (2016), who report an average boost of 1.09–1.1 for these fields without SMG the average is 0.90 dex, while for those fields with SMG the average is 0.2 dex). The temperatures estimated for the cold dust in the diffuse ISM are sensitive to the Herschel SPIRE colours, and as expected, these are also biased in the fits to H-ATLAS-only photometry in the fields with SMG. In Table 10, $T_{500}$ is the cold ISM temperature from MAGPHYS for the fits to Herschel-only photometry, while $T_{500}$ are the temperatures from fits including the ALMA photometry, and having corrected the Herschel fluxes for SMG contamination. The average temperature is $T_{500} = 22.2 \pm 2.4 \pm 2.4 \pm 2.4 (\text{median } 21.6 \text{K})$, while that with ALMA $850\mu m$ data and corrected fluxes is $T_{850} = 24.4 +0.8 \text{K (median } 24.5 \text{K)}$. Part of this effect is independent of any boosting by SMG and is due to the lower signal to noise at the $350$ and $500\mu m$ wavelengths compared to $250\mu m$ in the Herschel photometry. The long-wavelength ALMA flux constrains the cold
This was then compared to the CO luminosities and calibrations for fluxes in conjunction with ALMA 850 μm data because the ALMA data. Those which include the ALMA data.

Herschel L. Dunne et al. (in preparation) show that the average of the literature, Dunne et al. (in preparation) show that the average dust mass from MAGPHYS is larger than that on much larger in fields with SMG (0.36 versus 0.11). The effect on the derived dust mass from MAGPHYS is larger than that on L_{850 \text{SED}} because the dust mass is sensitive to temperature as well as the overall flux, and the temperatures from the Herschel-only fits are lower than those which include the ALMA data.

The effect of the flux boosting on the SED fits is much smaller once ALMA data are present because the ALMA 850 μm data force such a tight constraint on the SED shape. Using uncorrected SPIRE fluxes in conjunction with ALMA 850 μm data produces differences in SED parameters which are well within the 1σ errors (Δ < 0.03 dex in L_{850}, Δ < 0.1 dex in M_δ, Δ < 0.1 dex in sSFR, and Δ < 1 K in T_{e}). Therefore, the boosting corrections are not so important as long as the high-resolution long wavelength data are present; however without ALMA data, the lack of boosting correction may lead to large biases in analyses of Herschel samples. For example, the VALSES survey (Villanueva et al. 2017) was an ALMA CO(1-0) follow-up of 160 μm selected H-ATLAS sources in the redshift range 0.1 < z < 0.4. In one paper (Hughes et al. 2017) the H-ATLAS photometry was fitted using MAGPHYS and the SED extrapolated to give L_{850 \text{SED}}(500 μm). This was then compared to the CO luminosities and calibrations for the dust-to-ISM mass factor α_{850} derived. However, in a re-analysis of the literature, Dunne et al. (in preparation) show that the average L_{850} / L_{CO} from VALSES is 0.2 dex lower than any other sample of low or high redshift sources, including this z = 0.35 sample. We expect that this offset in L_{850} / L_{CO} is due to the lensing magnification boosting effect shown in this work. Table 10 shows that the difference in L_{850 \text{SED}} inferred with and without the ALMA data is of this order. Other analyses potentially affected by this bias are the evolution of the 350 and 500 μm luminosity and dust mass functions (Dunne et al. 2011; Marchetti et al. 2016), modelling of the 350 and 500 μm source counts (Clements et al. 2010; Béthermin et al. 2012; Valiante et al. 2016), SED evolution (e.g. Symeonidis et al. 2013; Viero et al. 2013), and stacking analyses (e.g. Bourne et al. 2012; Viero et al. 2013; Schreiber et al. 2015). In particular, the stacking analyses of both Bourne et al. (2012) and Viero et al. (2013) found that the dust temperatures decreased with stellar mass in the lowest redshift bin (as we would predict based on the extra boosting at 350 and 500 μm due to the cosmic lensing bias). In Bourne et al. (2012), a strong increase in the stacked 500 μm luminosity of optically red (passive) galaxies was also seen from z = 0–0.35. A strong lensing explanation did not seem to explain those findings at that time, but the possibility of the lensing bias reported here and in González-Nuevo et al. (2014) was not known at that time. A strongly evolving optically red population which had optical spectral signatures (in stacks) of both old stellar populations and ongoing SF was found in Eales et al. (2018) using the H-ATLAS catalogues. Could these optically red sources with strongly evolving dust emission be sign-posting the haloes producing the magnification lensing bias?

A larger sample of 0.2 < z < 0.7 galaxies selected at 250 μm and imaged with ALMA will be required to understand and address these issues, and to determine the statistics of boosting due to this effect in bins of redshift and stellar mass.

4.3 Summary of flux boosting and its implications

In summary, the 250 μm flux is the least affected of the SPIRE bands by the presence of a background SMG because (i) the beam size increases with increasing wavelength, and (ii) the K-correction favours means that high redshift sources are relatively brighter at the longer wavelengths. The practical consequences of the contaminant sources are thus:

(i) The SMG in the Herschel beam boosts the 250 μm flux of the z = 0.35 galaxy; in cases near the threshold for detection this could push the z = 0.35 source into the H-ATLAS catalogue. This effect results in an increased probability to find a nearby background SMG for 250 μm sources close to the detection limit.

(ii) The lensing explanation for the overdensity of SMG in these fields is not weakened by the boosting effect, but the parameters derived from the modelling would be affected. This is beyond the scope of this study.

(iii) The SMG in the beam reddens the Herschel sub-mm colours of the target galaxy, making them relatively brighter at 350 and 500 μm than they would have been without the contaminant. This mimics the effect of colder dust in the SED and leads to an underestimate of the cold dust temperature in MAGPHYS or two-component MBB fitting. For single MBB fits, it would result in a lower value for β, if that were a free parameter.

(iv) There are likely to be significant overestimates of sub-mm fluxes if they are estimated by extrapolating SEDs fitted to Herschel fluxes which have been boosted in this way.

(v) The combination of flux-boosting and reddening of the SED means that M_δ and L_{850 \text{SED}} can be biased high by 0.15–0.25 dex for samples affected by this process: 350–850 μm sources 0.2 < z < 0.7 measured with large beams.

5 CONCLUSIONS

We present serendipitous detections of high redshift dusty galaxies in ALMA 850 μm images of a complete sample of twelve z = 0.35 galaxies, selected at 250 μm from the H-ATLAS survey.

Table 10. The difference in SED fitted parameters when using Herschel-only photometry compared to the corrected Herschel+ ALMA data.

| Name | SMG | T_{850} | T_{500} | Δ M_δ | Δ L_{850 \text{SED}} |
|------|-----|---------|---------|-------|------------------|
| 163  | N   | 22.5    | 21.6    | 0.07  | 0.08             |
| 3132 | N   | 25.9    | 22.4    | 0.19  | 0.15             |
| 5523 | N   | 21.8    | 16.5    | 0.53  | 0.45             |
| 5526 | N   | 24.4    | 25.6    | 0.10  | 0.08             |
| 6216 | N   | 20.0    | 20.3    | -0.05 | -0.1             |
| 6451 | N   | 25.0    | 25.7    | 0.03  | 0.06             |
| 1160 | Y   | 28.3    | 21.5    | 0.66  | 0.32             |
| 2173 | Y   | 24.5    | 19.7    | 0.40  | 0.26             |
| 3366 | Y   | 26.5    | 20.2    | 0.71  | 0.58             |
| 4104 | Y   | 27.7    | 25.4    | 0.22  | 0.06             |
| 5347 | Y   | 19.9    | 20.4    | 0.03  | 0.02             |
| 6418 | Y   | 23.4    | 21.7    | 0.14  | 0.001            |

Note. Sources are grouped as to whether they have a SMG detected in the field at 850 μm. T_{850} is the cold dust temperature fitted by MAGPHYS using the 850 μm ALMA data and making corrections for blending as described in Section 4. T_{500} is the temperature fitted to the catalogue H-ATLAS photometry only with no corrections. Δ M_δ is the difference in log M_δ between the H-ATLAS only and corrected H-ATLAS + 850 μm photometry. Δ L_{850 \text{SED}} is the difference in log L_{850 \text{SED}} from the best-fitting MAGPHYS SED in the H-ATLAS only and corrected H-ATLAS + 850 μm cases. \dagger SDP5323 has no PACS coverage and therefore its SED is very poorly constrained without the ALMA data point. We do not use this source in the analysis of average properties.
(i) Half of the ALMA Band 7 fields contained one or more high redshift SMG, an overdensity of a factor 4–6 relative to the background counts.

(ii) We compared the statistics for the SMG with models of the lensing effect of group scale haloes finding a remarkably good agreement, both in terms of the cross-correlation signal and the correlation between galaxies in haloes with interacting satellites and the presence of SMG. Thus lensing is certainly a plausible explanation for the excess SMG detected around these sources.

(iii) These extra SMG contribute significantly to the SPIRE 350 and 500 μm in some cases. We derive average flux-boosting factors of 1.13, 1.26, and 1.44 for the 250, 350, and 500 μm SPIRE bands for this group of 12 representative 250 μm sources at $z = 0.35$ from H-ATLAS. These are significantly larger corrections at 350 and 500 μm than estimated by Valiante et al. (2016) who used simulations which did not include lensing between low and high-redshift sources. A boosting correction related to lensing is likely to be dependent on the redshifts of the target sources, as the probability for lensing depends on the lens-source geometry. For $z < 0.1$ the lensing probability is much lower, but from $z = 0.2–0.7$ it is likely that this sample is reasonably representative. Larger samples at different redshifts would be required to investigate this further.

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DATA AVAILABILITY

The data underlying this article are publicly available from the ALMA archive http://almascience.eso.org/aq/ using the project code 2012.1.00973.S.

REFERENCES

Almaini O., Dunlop J. S., Willott C. J., Alexander D. M., Bauer F. E., Liu C. T., 2005, MNRAS, 358, 875
Aretxaga I. et al., 2011, MNRAS, 415, 3831
Baldry I. K. et al., 2018, MNRAS, 474, 3875
Bethermin M., Smail I., Béthermin M., 2012, A&A, 542, A58
Bethermin M. et al., 2020, A&A, preprint (arXiv:2002.00962)
Blain A. W., 1997, MNRAS, 290, 553
Blain A. W., Kneib J. P., Ivison R. J., Smail I., 1999, ApJ, 512, L87
Bonavera L. et al., 2019, J. Cosmol. Astropart. Phys., 9, 21
Bourne N. et al., 2012, MNRAS, 421, 3027
Bourne N. et al., 2014, MNRAS, 444, 1884
Bourne N. et al., 2016, MNRAS, 462, 1714
Bussmann R. S. et al., 2015, ApJ, 812, 43
Cañameras R. et al., 2015, A&A, 581, A105
Cavuoti S. et al., 2015, MNRAS, 452, 3100
Chapman S. C., Blain A. W., Smail I., Ivison R. J., 2005, ApJ, 622, 772
Child H. L., Habib S., Heitmann K., Frontiere N., Finkel H., Pope A., Morozov V., 2018, ApJ, 859, 55
Clements D. L. et al., 2010, A&A, 518, L8
Combes F., García-Burillo S., Braine J., Schinnerer E., Walter F., Colina L., 2011, A&A, 528, A124
Cowie L. L., Barger A. J., Kneib J. P., 2002, AJ, 123, 2197
du Cunha E., Charlot S., Elbaz D., 2008, MNRAS, 388, 1595
du Cunha E. et al., 2015, ApJ, 806, 110
de Jong J. T. A. et al., 2017, A&A, 604, A134
Driver S. P. et al., 2011, MNRAS, 413, 971
Driver S. P. et al., 2016, MNRAS, 455, 3911
Dunne L. et al., 2011, MNRAS, 417, 1510
Dutton A. A., Macciò A. V., 2014, MNRAS, 441, 3359
Eales S. et al., 2010, PASP, 122, 499
Eales S. et al., 2018, MNRAS, 473, 3507
Edge A., Sutherland W., Kuijken K., Driver S., McMahon R., Eales S., Emerson J. P., 2013, Messenger, 154, 32
Fujimoto S., Ouchi M., Shibuya T., Nagai H., 2017, ApJ, 850, 83
González-Nuevo J. et al., 2014, MNRAS, 442, 2680
González-Nuevo J. et al., 2017, J. Cosmology Astropart. Phys., 2017, 024
Graham J. R., Liu M. C., 1995, ApJ, 449, L29
Griffin M. J. et al., 2010, A&A, 518, L3
Harris A. I. et al., 2012, ApJ, 752, 152
Hildebrandt H. et al., 2013, MNRAS, 429, 3230
Hodge J. A. et al., 2016, ApJ, 833, 103
Hui L.-Y., Cowie L. L., Chen C.-C., Barger A. J., Wang W.-H., 2016, ApJ, 829, 25
Hughes T. M. et al., 2017, MNRAS, 468, L103
Hurley P. D. et al., 2017, MNRAS, 464, 885
Ivison R. J. et al., 2016, ApJ, 832, 78
Jarugula S. et al., 2019, ApJ, 880, 92
Knudsen K. K., van der Werf P. P., Kneib J. P., 2008, MNRAS, 384, 1611
Kraft R. P., Burrows D. N., Nousek J. A., 1991, ApJ, 374, 344
Lang P. et al., 2019, ApJ, 879, 54
Lapi A., Negrello M., González-Nuevo J., Cai Z. Y., De Zotti G., Danese L., 2012, ApJ, 755, 46
Liske J. et al., 2015, MNRAS, 452, 2087
Maddox S. J., Dunne L., 2020, MNRAS, 493, 2363
Marchetti L. et al., 2016, MNRAS, 456, 1999

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APPENDIX A: SIZE FITTING PROCEDURE

For the $u$, $v$ source fitting, we use the CASA task UVMODELFIT with a 2D Gaussian model. The model is described by six parameters: the flux $S_{\nu}$, position in RA and Dec, major axis size $\theta_{m1}$, P.A., and the axial ratio $b/a$. For our data, the axial ratio is very poorly constrained and this led to a bias towards an axial ratio very close to zero, usually between 0.1 and 0.2 for disc galaxies. For a randomly oriented distribution of discs the expectation value of $\sin i$ is 0.5, which gives $(b/a) = 0.753$. We therefore fitted the model to the data with the axial ratio fixed at $b/a = 0.753$ and these parameters are listed in Table 6.

The range of possible unknown disc orientations will contribute to the uncertainties of the other parameters, even though we have fixed the axial ratio in the fit. The upper and lower 1-$\sigma$ ranges of $b/a$ from the distribution of disc orientations are represented by the 16th and 84th percentiles ($b/a = 0.549, 0.987$) respectively. To estimate the total uncertainties, we fit the model with $b/a$ fixed to its 16th and 84th percentile values, and use the resulting parameters to set the 1-$\sigma$ upper and lower bounds on $\theta_{m1}$ and $S_{\nu}$. We then add this error in quadrature to the quoted fitting errors, $\delta x(fit)$ to arrive at our best estimate of the uncertainties:

$$\frac{\delta \theta_{m1}(tot)}{\theta_{m1}} = \sqrt{\left(\frac{\delta \theta_{m1}(fit)}{\theta_{m1}}\right)^2 + \left(\frac{\theta_{m1}(84) - \theta_{m1}(16)}{2 \theta_{m1}}\right)^2}$$

with a similar formalism for the other two parameters, $S_{\nu}$ and $\theta_{m2}$ (which is simply the axial ratio times the major axis).

In the majority of cases, the variation of $b/a$ from the 16th–84th percentile range causes little extra variation in $\theta_{m1}$ or $S_{\nu}$, and so the quoted parameter is rather insensitive to the exact value of axial ratio (1–3 percent in flux and 10–20 percent for major axis). For two sources (SDP.4104, SDP.5347), there is a larger sensitivity (5–7 percent in flux and 23–62 percent in major axis), this is reflected in larger errors on the parameters.

APPENDIX B: NOTES ON INDIVIDUAL FIELDS

**SDP.1160**

There are two bright SMG in this field located 5 and 12.5 arcsec from the optical galaxy (Fig. 3); neither have a counterpart in the VIKING $K$-band catalogue. There is also a 500 $\mu$m $Herschel$ source 28.5 arcsec to the South that is identified in the H-ATLAS ‘red source’ catalogue, which uses a subtractive method to recover sources which are very faint at 250 $\mu$m but brighter at 500 $\mu$m (Ivison et al., 2016). The H-ATLAS red source contributes 4.5 mJy to the 500 $\mu$m flux for SDP.1160. This source is outside the Band 7 imaged area, but searching in the Band 3 cube we find tentative evidence for two 3-mm line sources at similar redshift at the position of the 350 and 500 $\mu$m peaks, see Table C1. Combining the line information with the SPIRE colours (using the red source catalogue fluxes) we find that the most plausible redshift is $z = 4.4–4.8$ with the lines being either CO(4–3) or [CI](3P1-3P0). A very bright 850 $\mu$m source with a flux of 8–12 mJy would be expected in this scenario, or a number of weaker sources which together produce the red $Herschel$ colours, such as those found by Oteo et al. (2018).

**SDP.2173**

There is an SMG in this field located 7.5 arcsec from the optical galaxy, which has a $K$-band counterpart ($K_{AB} = 21.45$) clearly visible in the VIKING $K$-band image (Fig. 3 and Table 6). No 3-mm continuum or lines are detected at the location of the SMG.
Too much of a good thing?

SDP.3366

The $z = 0.35$ galaxy is interacting with a smaller companion to the North-East, as evidenced from the [C\text{I}] kinematics. Slightly further north we find strong 850 $\mu$m continuum emission from an SMG coincident with a very red source ($K_{AB} = 19.0$) located 3.4 arcsec to the north-east of the $z = 0.35$ galaxy (Fig 3). There is a second, fainter, candidate SMG ($4–5\sigma$) just to the left of first, which is listed in Table C1 as 3366.s2. No 3-mm continuum or lines are detected at the location of the SMG.

SDP.4104

The $z = 0.35$ galaxy is interacting with a similar sized companion, as evidenced by the CO and [C\text{I}] kinematics. There is a bright SMG in this field located 7.2 arcsec from the largest member of the pair, which has $K_{AB} = 20.7$ (see Fig. 3). No 3 mm continuum or lines are detected at the location of the SMG.

SDP.5347

The $z = 0.35$ galaxy is interacting with several small satellites, leaving a tidal trail of CO, [C\text{I}], and some dust to the western side of the galaxy. There is a 850 $\mu$m continuum source to the north-east, which we assume to be a high redshift SMG; details are presented in Table 6 and Fig. 3. There is a faint whiff of $K$-band emission in a highly smoothed image, and no 3 mm continuum or line detection.

SDP.6418

The $z = 0.35$ galaxy is interacting with a smaller neighbour, as evidenced by the [C\text{I}] kinematics. The SMG in this image is strong enough for self-calibration. There is no $K$-band counterpart and no 3 mm or line emission detected.

SDP.6451

The SPIRE colours of this source are most definitely contaminated, as is obvious when attempting an SED fit. We searched the data set for any evidence of sources which may be contributing to the red SPIRE colours and find two potential candidates, which are listed in Table C1. 6451.s1 is a 4.9$\sigma$ 850 $\mu$m source, which is only just below the threshold we consider for calculation of the number counts. 6451 refers to a potential 3-mm line source, which just overlaps the B7 fov giving an upper limit to the 850 $\mu$m flux. These are not considered in the overdensity calculation but listed in the Appendix for further information.

APPENDIX C: CANDIDATE HIGH REDSHIFT SOURCES

| SMG     | R.A.   | Dec.     | $S_{850}$ (mJy) | SNR | $r$ (arcsec) | $K_{AB}$ |
|---------|--------|----------|-----------------|-----|-------------|---------|
| 3366.s2 | 09:04:50.31 | $-00:12:00.17$ | $0.33 \pm 0.082^d$ | 5.1 | point | $4.2 < 21.32$ |
| 6451.s1 | 09:08:50.0 | $+02:26:00.85$ | $0.68 \pm 0.14$ | 4.9 | 8.7 | $<21.32$ |

| SMG     | R.A.   | Dec.     | $S_{\text{line}}$ | $\sigma_{\text{line}}$ | $r$ (arcsec) | $K_{\text{AB}}$ | $\nu_{\text{line}}$ |
|---------|--------|----------|--------------------|------------------------|-------------|-------------|-----------------|
| 1160.l1 | 09:00:29.32 | $+01:21:46.8$ | 2.83 | 0.76 | 30 | $<21.32$ | 85.25 |
| 1160.l2 | 09:00:28.86 | $+01:21:45.1$ | 0.62 | 0.12 | 30 | $<21.32$ | 85.485 |
| 5347.l1 | 09:06:59.22 | $+02:02:20.74$ | 1.73 | 0.52 | 26.9 | $<21.32$ | 85.948 |
| 5347.l2 | 09:06:59.14 | $+02:02:17.17$ | 0.52 | 0.17 | 20.7 | $<21.32$ | 85.948 |
| 6451.l1 | 09:08:48.6 | $+02:26:00.8$ | 1.64 | 0.37 | 13 | $<21.32$ | 99.1678 |
| 6451.l2 | 09:08:49.3 | $+02:25:59.3$ | 1.95 | 0.57 | 4 | $<21.32$ | 99.509 |

Note. Line candidates at 3 mm. There is no continuum imaging at 850 $\mu$m at the location of the SDP 1160 line candidates. Plausible line identifications are: $z = 3.06$ CO(3–2), $z = 4.4/4.77$ CO(4–3)/[C\text{I}](3P1-3P0), and $z = 5.76$ CO(5–4), but only the $z = 4.5–4.8$ solutions fit well with the SPIRE colours.

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