TYPE II-P SUPERNOVAE FROM THE SDSS-II SUPERNOVA SURVEY AND THE STANDARDIZED CANDLE METHOD*

Chris B. D'Andrea1, Masao Sako1, Benjamin Dilday2, Joshua A. Frieman3,4,5, Jon Holtzman6, Richard Kessler3,4, Kohki Konishi4, D. P. Schneider6, Jesper Sollerman6,10,11, Craig Wheeler11, Naoki Yasuda7, David Cinabro12, Saurabh Jha2, Robert C. Nichol13, Hubert Lamperti13, Matthew Smith13,14, David W. A. Atlee15, Bruce Bassett14,16, Francisco J. Castander17, Ariel Goobar18,19, Ramon Miquel20,21, Jakob Nordin18,19, Linda Östman18,19, José L. Prieto22,27, Robert Quimby23, Adam G. Riess24,25, and Maximilian Stritzinger26

1 Department of Physics and Astronomy, University of Pennsylvania, 209 South 33rd Street, Philadelphia, PA 19104, USA; cdandrea@physics.upenn.edu
2 Department of Physics and Astronomy, Rutgers University, 136 Frelinghuysen Road, Piscataway, NJ 08854, USA
3 Kavli Institute for Cosmological Physics, University of Chicago, 5640 South Ellis Avenue, Chicago, IL 60637, USA
4 Department of Astronomy and Astrophysics, University of Chicago, 5640 South Ellis Avenue, Chicago, IL 60637, USA
5 Center for Particle Astrophysics, Fermi National Accelerator Laboratory, P. O. Box 500, Batavia, IL 60510, USA
6 Department of Astronomy, MSC 4500, New Mexico State University, P. O. Box 30001, Las Cruces, NM 88003, USA
7 Institute for Cosmic Ray Research, University of Tokyo, 5-1-5, Kashiwanoha, Kashiwa, Chiba, 277-8582, Japan
8 Department of Astronomy and Astrophysics, 525 Davey Laboratory, Pennsylvania State University, University Park, PA 16802, USA
9 Dark Cosmology Centre, Niels Bohr Institute, University of Copenhagen, Juliane Maries Vej 30, DK-2100 Copenhagen Ø, Denmark
10 The Oskar Klein Centre, Department of Astronomy, AlbaNova, Stockholm University, SE-106 91 Stockholm, Sweden
11 Department of Astronomy, McDonald Observatory, University of Texas, Austin, TX 78712, USA
12 Department of Physics and Astronomy, Wayne State University, Detroit, MI 48202, USA
13 Institute of Cosmology and Gravitation, Dennis Sciama Building, Burnaby Road, University of Portsmouth, Portsmouth PO1 3FX, UK
14 Department of Mathematics and Applied Mathematics, University of Cape Town, Rondebosch 7701, South Africa
15 Department of Astronomy, Ohio State University, 140 West 18th Avenue, Columbus, OH 43210, USA
16 South African Astronomical Observatory, P.O. Box 9, Observatory 7935, South Africa
17 Institut de Ciències de l’Espai, (IEEC - CSIC), Campus UAB, 08193 Bellaterra, Barcelona, Spain
18 Department of Physics, Stockholm University, AlbaNova University Center, SE-106 91 Stockholm, Sweden
19 The Oskar Klein Centre for Cosmoparticle Physics, Department of Physics, AlbaNova, Stockholm University, SE-106 91 Stockholm, Sweden
20 Instituto Catalana de Recerca i Estudis Avançats, Barcelona, Spain
21 Institut de Física d’Altes Energie, E-08193 Bellaterra, Barcelona, Spain
22 Carnegie Observatories, 813 Santa Barbara St., Pasadena, CA 91101, USA
23 Department of Astronomy, California Institute of Technology, Pasadena, CA 91125, USA
24 Space Telescope Science Institute, 3700 San Martin Drive, Baltimore, MD 21218, USA
25 Department of Physics and Astronomy, Johns Hopkins University, 3400 North Charles Street, Baltimore, MD 21218, USA
26 Las Campanas Observatory, Carnegie Observatories, Casilla 601, La Serena, Chile

ABSTRACT

We apply the Standardized Candle Method (SCM) for Type II Plateau supernovae (SNe II-P), which relates the velocity of the ejecta of a SN to its luminosity during the plateau, to 15 SNe II-P discovered over the three season run of the Sloan Digital Sky Survey-II Supernova Survey. The redshifts of these SNe—0.027 < z < 0.144—cover a range hitherto sparsely sampled in the literature; in particular, our SNe II-P sample contains nearly as many SNe in the Hubble flow (z > 0.01) as all of the current literature on the SCM combined. We find that the SDSS SNe have a very small intrinsic I-band dispersion (0.22 mag), which can be attributed to selection effects. When the SCM is applied to the combined SDSS-plus-literature set of SNe II-P, the dispersion increases to 0.29 mag, larger than the scatter for either set of SNe separately. We show that the standardization cannot be further improved by eliminating SNe with positive plateau decline rates, as proposed in Poznanski et al. We thoroughly examine all potential systematic effects and conclude that for the SCM to be useful for cosmology, the methods currently used to determine the Fe II velocity at day 50 must be improved, and spectral templates able to encompass the intrinsic variations of Type II-P SNe will be needed.

Key words: cosmology: observations – distance scale – supernovae: general – surveys

Online-only material: color figures, supplementary data file

1. INTRODUCTION

Type Ia supernovae (SNe Ia) are standardized candles; although their peak magnitudes can vary by up to ~2.5 mag, empirical relations between the shape of their light curves and peak magnitude result in distance measurements that can be accurate to ~7% (Phillips 1993; Jha et al. 2007; Guy et al. 2007). This standardization has proven to be invaluable, as observations of SNe Ia led to the discovery of the accelerating expansion of the universe (Riess et al. 1998; Perlmutter et al. 1999). Dedicated surveys have now observed over a thousand of these objects in the past several years over a wide range of redshifts, lowering statistical uncertainties with the volume of their discoveries (for high redshift SN programs, see Riess et al. 2004, 2007; Astier et al. 2006; Wood-Vasey et al. 2007; Miknaitis et al. 2007; Kessler et al. 2009a; Frieman et al. 2008; for low redshift, see Filippenko et al. 2001; Hamuy et al. 2006; Aldering et al. 2002;
Hicken et al. (2009). As a result, selection effects and other potential sources of bias are of increasing importance to improving the constraints on the dark energy equation of state. In order to fully utilize future surveys that will discover very large numbers of SNe (DES28; LSST29), these systematic uncertainties will have to be reduced.

Type II Plateau Supernovae (SNe II-P) can also be used as distance indicators, though thus far with less precision and to much lower distances than SNe Ia. SNe II-P are objects that, observationally, are classified as Type II SNe by the presence of hydrogen absorption in their spectra, and as “Platue” based on the slow decay of their early light curves (Barbon et al. 1979). Distance measurements using the Expanding Photosphere Method (EPM; see Kirshner & Kwan 1974; Schmidt 1993; Eastman et al. 1996) and the more recent, related Spectral Expanding Atmosphere Method (SEAM; see Baron et al. 2004; Dessart & Hillier 2006), which are based on the modeling of the SN atmosphere, have been shown to recover distances to 10% precision (Dessart et al. 2008). A different approach has been taken by Hamuy & Pinto (2002, hereafter HP02), who have shown that SNe II-P magnitudes can also be standardized empirically, despite being far more heterogeneous (peak luminosity dispersion of more than 5 mag; see Patat et al. 1994; Pastorello et al. 2004) than SNe Ia. The theoretically based methods take advantage of the relative simplicity of modeling hydrogen, which dominates the atmosphere of SNe II-P, as compared to the intermediate mass elements that make up the ejecta of SNe Ia. SNe II-P also differ from their brighter brethren in a couple of other advantageous ways. Over the past decade, observations in archival pre-SNe II-P images have found red supergiants in the mass range 7–16 $M_\odot$ (Van Dyk et al. 2003; Smartt et al. 2004; Maund et al. 2005; Maund & Smartt 2005; Hendry et al. 2006; Li et al. 2006, 2007; Mattila et al. 2008), and recently it has been shown that at least one of these cases, the supposed progenitor is no longer present after the SN II-P has dimmed (Maund & Smartt 2009). So, compared to SNe Ia, where there is still uncertainty over the progenitor system (or systems), SNe II-P explosions are better understood. Also, since SNe II-P have only been found in late-type galaxies—unlike SNe Ia, which are found in both late- and early-type galaxies—it is likely that biases from environmental effects will have a smaller effect on distance measurements for SNe II-P than SNe Ia. Thus, the differences between the two types of SNe and their methods of standardization will result in different systematic effects, allowing SNe II-P to serve as a useful check on SNe Ia measurements.

The standardization of the SNe II-P luminosity was introduced by HP02, who found that the luminosity and the expansion velocity at the photosphere are correlated when the SN is in its plateau phase; they use 50 rest-frame days post explosion as a convenient reference epoch to compare across SNe (this epoch is late enough to ensure the SN has entered the plateau phase, while still before it leaves the plateau). The origin of this relationship is strongly grounded physically; a more luminous supernova’s hydrogen recombination front will be at a greater distance from the core than in a less luminous SN, and thus the velocity of matter at the photosphere will be greater. Using the velocity of the ejecta as measured from the minimum of the Fe $\text{ii} \lambda5169$ absorption feature and a reddening correction based on the color of the SN when its light curve falls off the plateau, they found that the scatter in the Hubble diagram for $V$ and $I$ magnitudes drops from 0.95 and 0.80 mag, respectively, to 0.39 and 0.29 mag. When they then restricted their sample to the 8 SNe with $z < 0.01$ in order to reduce the effect of peculiar velocities on host galaxy redshift, the scatter of their sample dropped even further, to 0.20 mag in $V$ and 0.21 mag in $I$. This technique has come to be known as the Standardized Candle Method (SCM).

Nugent et al. (2006, hereafter N06) improved upon the HP02 method in several ways that address its limitations for application to SNe at cosmological distances. The HP02 host galaxy extinction correction is replaced by the rest-frame $V - I$ color at day 50, which can be obtained with less extensive late time photometric monitoring. To allow spectroscopic follow-up programs to be more flexible, they also derive an observational relationship between the velocity of the Fe $\text{ii}$ line at epochs spanning days 9–75 to the velocity at day 50, which is crucial for any realistic spectroscopic follow-up program. They apply the standardization method to five high-redshift (0.13 < $z$ < 0.29) SNe obtained as part of the Supernova Legacy Survey (SNLS; Astier et al. 2006), as well as one at $z = 0.019$ followed up by the Caltech Core-Collapse Project (CCCP; Gal-Yam et al. 2007; SN 1999gi, which was added to the data set of SNe II-P by Hamuy 2003, is also included). The result of their SNLS-only fit differed strongly from that of the low-redshift SNe in HP02, which was attributed to a number of factors, including a small sample size, differences in data analysis techniques, and observational biases. Their data did confirm, however, that the relation between ejecta velocity and magnitude could be used to reduce the intrinsic dispersion in the sample.

Olivares (2008) applied the SCM to 37 SNe II-P, for which they use 30 days before the end of the plateau as the common epoch of reference. They find the Hubble Diagram dispersion to be remarkably similar whether one uses $B$, $V$, or $I$-band magnitudes (0.28, 0.31, and 0.32 mag, respectively), and raise the possibility that the magnitude–velocity relation may be quadratic instead of linear.

The most recent work on SNe II-P standardization was done by Poznanski et al. (2009, hereafter P09), which presented new data on 19 low-redshift (all located at $z < 0.03$) SNe II-P with multi-epoch spectra. These SNe were discovered as part of the Lick Observatory SN Search (Filippenko et al. 2001) by the Katzman Automatic Imaging Telescope (KAIT). The most significant advancement of the SCM presented in P09 is the introduction of a robust technique for determining the velocity of the ejecta by cross-correlating the observed spectra with high-quality SNe II-P templates contained in SuperNova Identification Code (SNID; see Blondin & Tonry 2007; Tonry & Davis 1979). As mentioned in P09, the velocity of the weak, broad Fe $\text{ii}$ line is difficult to measure without introducing systematic offsets that hinder comparisons across multiple data sets. Using the SCM, they found a significantly larger $I$-band scatter (0.38 mag) in their Hubble diagram than either HP02 or N06 (including all objects from both previous works), but showed that by removing all SNe with a positive plateau decline rate (defined as a decrease in brightness in $I$-band magnitude between days 10 and 50) from their analysis, the dispersion of this “culled” sample was only 0.22 mag, or ~10% in distance.

In this work, we apply the SCM to both the 15 new SNe II-P from the SDSS-II Supernova Survey and the combined set of our SNe plus those in the literature. Our sample fills in a redshift gap between $z<0.027$ and $z<0.144$, that has very few other objects. We discuss our observations in Section 2, and present light curves for these SNe and an additional 19 spectroscopically confirmed

28 https://www.darkenergysurvey.org
29 http://www.lsst.org/lsst
SNe II-P, also discovered during the SDSS-II Supernova Survey, for which we do not have sufficient data to include in our SCM sample. We also discuss how we determine which SNe are part of the SCM sample. In Section 3 we explain in detail our process for determining K- and S-corrections, and explore how these are affected by the uncertainty in the explosion date and the choice of spectral template. We analyze the spectra of our SNe in Section 4, and obtain their ejecta velocity at day 50. In Section 5 we present the results from combining our observed SNe with those of HP02, N06, and P09, and applying the SCM to a combined sample of 49 SNe II-P. We discuss our results and their interpretations in Section 6, and conclude with an eye toward what will be needed for future SNe II-P campaigns in Section 7.

2. OBSERVATIONS

The Sloan Digital Sky Survey-II Supernova Survey (Frieman et al. 2008, hereafter SDSS-SNS) was one of three parts of the SDSS-II project. The SDSS-SNS repeatedly surveyed the 300 deg² Southern Equatorial Stripe (designated stripe 82; see Stoughton et al. 2002) during the Fall seasons (September 1–November 30) of 2005–2007 using a dedicated 2.5 m telescope at Apache Point Observatory, New Mexico (Gunn et al. 2006). Each photometric observation consists of nearly simultaneous 55 s exposures in each of the five ugriz filters (Fukugita et al. 1996) using the wide-field SDSS CCD camera (Gunn et al. 1998). High-quality light curves were obtained (Holtzman et al. 2008) on a photometric system calibrated to an uncertainty of 1% (Ivezić et al. 2004). For a technical summary of the SDSS, see York et al. (2000); further information can be found in Hogg et al. (2001), Smith et al. (2002), Pier et al. (2003), Tucker et al. (2006), and Abazajian et al. (2009).

Supernova candidates were fit to model light curves of SNe 1a, SNe Ib/c, and SNe II, and photometrically classified by their most probable type; see Sako et al. (2008). The main science driver of the SDSS-SNS was Type Ia SNe, so the spectroscopic follow-up program was designed to achieve high efficiency in following up these objects; only in the third season, when the work presented here began, did obtaining spectra of SNe II-P candidates become an explicit objective. Spectroscopic observations of SNe II-P were performed by the 9.2 m Hobby–Eberly Telescope (HET) at McDonald Observatory, 3.6 m New Technologies Telescope (NTT), the 3.5 m Astrophysical Research Consortium Telescope at Apache Point Observatory, the 8.2 m Subaru Telescope, the 2.4 m Hiltner Telescope at MDM Observatory, the 4 m Mayall Telescope at Kitt Peak National Observatory, the Magellan 6.5 m Clay Telescope, the 4.2 m William–Herschel Telescope, the 2.6 m Nordic Optical Telescope, and the 3.6 m Telescopio Nazionale Galileo (TNG). Spectroscopic typing and redshift determination for each SN candidate is discussed in C. Zheng et al. (2010, in preparation); redshifts based on host galaxy spectra are accurate to Δz = 0.0005, and those based on SN spectral features are accurate to Δz = 0.005.

2.1. SCM Sample

The SDSS-SNS spectroscopically confirmed a total of 34 SNe II-P. We do not include objects that are likely to be SNe II-P but have an unclear spectroscopic identity; this exclusion has no impact on our final sample of useable SNe. To be classified as a SN II-P, the spectrum of the object must have identifiable hydrogen P Cygni lines, and lack the narrow emission lines particular to the SN IIn class. By finding all occasions where a SN candidate persists through more than one observing season, we eliminate from our sample any active galactic nuclei. Since no clear quantitative divide exists between the slowly declining SN II-P light curve and that of the more rapidly declining Linear class (SN II-L), we classify all of our remaining candidates as SNe II-P. It is worth noting that, although we do not use the light curve shape to define our classification as a SN II-P, all objects classified this way exhibit flat or slowly declining linear light curves.

Our SCM sample is composed of the SDSS-SNS SNe II-P that pass three cuts, each of which removes only those SNe that lack the necessary data for application to the SCM; we do not remove any SN because of its observed properties. The first cut, having an observational constraint on the explosion epoch, requires a null detection in the same observing season before the first detection of the SN (defined as 4σ in flux). This constraint eliminates all SNe II-P that are discovered in the first observation of each season. The second cut imposed is on the length of the plateau observed. To ensure an accurate derivation of the magnitude and color of each SN at day 50 (described in Section 3), three or more detections occurring at least 30 rest-frame days after the explosion—one of which must be at least 40 rest-frame days post-explosion—are required. We impose this cut after comparing the day 50 flux interpolated from our most well sampled SNe with what we would obtain using only epochs at t < 40 to extrapolate the day 50 flux, and finding that the latter result can differ from the former by up to 50%. The photometry cut effectively excludes all SNe discovered roughly within the last half of each observing season. The third requirement is that there be at least one spectrum taken between rest-frame days 9 and 75 that allows the Fe ii λ5169 velocity at day 50 to be determined; details of this process are described in Section 4. Since the nature of the spectroscopic follow-up program of the SDSS-SNS was primarily to determine the type of each supernova as early in its development as possible, the majority of our spectra are taken at early times (before the Fe ii line fully develops) and are of low signal to noise (since the objective of obtaining spectra was for typing, not analysis). The main exception to the spectroscopic observing strategy was a single night of observing at Subaru during the Fall 2007 observing run (when SN II-P follow-up had become a priority) where we obtained high-quality spectra for nine SNe II-P; six of these SNe passed our photometric cuts.

Applying these cuts to our observed SNe, we find 15 of the 34 spectroscopically confirmed SNe II-P have sufficient data for the SCM analysis, and thus form our SCM sample. The explosion date constraint eliminates six objects; the photometric constraint seven; and the spectroscopic constraint four. Two more high-redshift SNe are eliminated from our sample after their rest-frame I-band magnitudes are found to have an uncertainty greater than 1 mag. We present the light curves for the 34 spectroscopically confirmed SNe II-P discovered by the SDSS-SNS in Figures 1 and 2. Each of the 15 SNe that comprise the SCM sample as described above are labeled as such in these figures. Approximately 60% of the discovered SNe II-P are from the 2007 observing season; a change in the priority of these objects as spectroscopic targets is the reason for such a large percentage of our sample originating in one season. All of the spectra that we use in our SCM analysis are plotted in Figure 3. The spectra and photometry data for all 34 spectroscopically confirmed SNe II-P are available for public use through the
Figure 1. Observed light curves for SNe II-P from the 2005 (top) and 2006 (bottom) seasons of the SDSS-II Supernova Survey. Blue X’s are magnitudes in $u$ band, green diamonds are $g$, red triangles are $r$, brown circles are $i+1$, and black squares are $z+2$. The $x$-axis is the Modified Julian Date. The IAU name is given in the upper left of each box, and the redshift in the upper right. Each SN that passes the cuts for inclusion in the Standard Candle Method sample, detailed in Section 2.1, has the letters “SCM” printed beneath its redshift. If the SN is not included in our SCM sample, it is labeled as having failed the explosion epoch (exp), plateau photometry (phot), or spectroscopic (spec) cut, also described in Section 2.1. Only observations where the Scene Modeling Photometry (SMP; see Section 3) is deemed to be of good quality are plotted; see Holtzman et al. (2008) for a description of SMP. Magnitudes shown are asinh magnitudes (Lupton et al. 1999), with softening parameters given in Stoughton et al. (2002).

(A color version of this figure is available in the online journal.)

SDSS-SNS Web site, and are also included as supplementary data in the electronic edition of the journal.

3. REST-FRAME PLATEAU MAGNITUDES

In this section we determine the rest-frame magnitudes at day 50 for each SN II-P in our sample. First we determine the observed-frame magnitudes at day 50 through light curve fitting. $K$-corrections are performed to transform observed magnitudes to the rest frame; $S$-corrections (Stritzinger et al. 2002) are added to the $griz$ SDSS magnitudes to obtain the Bessell $BVRI$ magnitudes, which are required to compare our sample of SNe with those published by HP02, N06, and P09. The following describes the procedure we adopted.

The plateau of each SN is well described by a slow, linear evolution in magnitude; since we fit for the plateau in flux space, we model it as an exponential. We fit the model to our observed photometry for all epochs $t - t_0 > 30(1 + z)$, where $t_0$, the estimated time of explosion, is defined as the midpoint between the last pre-SN observation and the first detection epoch. We use rest-frame day 30 as the starting point for the plateau because the observed rate of decline of the light curves in magnitudes after this epoch is constant. We fit the plateau in the $griz$ filters only, excluding $u$ because its rapid decline precludes detections in this band for almost all of our SNe at late times; we show three examples of our plateau fits in Figure 4. Depending on how well

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30 http://sdssdp47.fnal.gov/sdsssn/photometry/SNIIP.tgz
sampled each light curve is, we either interpolate or extrapolate fluxes at rest-frame day 50, and then convert them to SDSS filter magnitudes in the AB system using the zero-point offsets from the native SDSS system (see Table 1 of Holtzman et al. 2008). We refer to these magnitudes throughout this paper as the day 50 magnitudes.

Next, we transform the day 50 SDSS griz magnitudes into rest-frame Bessell BVRI magnitudes. For each SN, a template SN II-P spectrum is redshifted from its rest frame to the observed frame, and then reddened using the Milky Way extinction value along the line of sight from Schlegel et al. (1998), the Cardelli et al. (1989, hereafter CCM) reddening law, and $R_V = 3.1$. Since we do not have sufficient spectroscopic coverage of our SCM sample SNe to create our own day 50 SN II-P spectral template, we adopt the SN template used in N06 (P. Nugent 2009, private communication). We then warp (Nugent et al. 2002) the template spectrum to match the day 50 SDSS magnitudes using a spline; finally the template is de-extincted and returned to its rest-frame wavelength scale. Rest-frame Bessell BVRI magnitudes in the Vega system are then directly computed from the spectrum, using the response functions of Moro & Munari (2000) and the synthetic magnitudes of Vega in the Bessell filters given in Table 19 of Kessler et al. (2009a). The procedure described here serves to both $K$- and $S$-correct our observations. We do not correct for host-galaxy extinction; since SNe II-P have similar colors along their plateau, the amount

Figure 2. Same as Figure 1, except for SNe discovered in the 2007 season. Note the much larger number of SNe, which is primarily a result of a more concerted spectroscopic campaign for SNe II-P during the 2007 season. The supernova labeled “18321” is listed by its internal SDSS-SNS identification number, as it has not at present been assigned an IAU name. The two SNe that have rest-frame, day 50 $I$-band uncertainties larger than 1 mag are 2007nl and 2007nv. (A color version of this figure is available in the online journal.)
Figure 3. Spectra used in the SCM analysis for each of the 15 SNe II-P in our sample. The spectra are shown in the observed frame, and the date listed for each SN is the number of days since explosion in the observer frame. The redshift of each SN increases from the bottom ($z = 0.027$) to the top ($z = 0.1444$) of the plot. We have masked galaxy emission lines in those cases where they were present. Each spectrum has identifiable P Cygni lines in H\(\alpha\) and H\(\beta\), although in some instances the weak Fe\(\text{II}\) \(\lambda 5169\) line cannot confidently be identified.

Figure 4. Observed SDSS-SNS light curves for SNe II-P at a range of redshifts. Blue diamonds are g-band magnitudes; green triangles are r-band magnitudes; red squares are i-band magnitudes; and brown circles are z-band magnitudes. For clarity, each light curve has been offset by an amount given on each plot. Magnitudes have not been K- or S-corrected, nor have these light curves been corrected for extinction. Magnitudes are the standard definition of magnitudes, not the asinh magnitudes defined in Holtzman et al. (2008) for SDSS SNe. Solid lines are the plateau fits for each band, the procedure for which is defined in Section 3. The dotted line denotes rest-frame day 50 at the redshift of each SN. (A color version of this figure is available in the online journal.)

of host galaxy extinction is encapsulated in the rest-frame color.

Since there are uncertainties in the explosion epoch, the day 50 magnitudes, and the redshift of each SN, we run a Monte Carlo (MC) simulation of the process described above to determine how the uncertainties on these parameters affect the rest-frame day 50 $BVRI$ magnitudes. Each iteration of the MC starts by selecting a date $t_{\text{exp}}$ for the explosion epoch from the range $t_0 - \Delta t < t_{\text{exp}} < t_0 + \Delta t$, where the uncertainty $\Delta t$ is half the difference between the last non-detection and the first detection of the SN and the probability distribution is described by a top hat function. Due to the high cadence of the SDSS-SNS, the median uncertainty in explosion date from detection constraints in our SCM sample is an exceptionally low 3.5 days, matched only by the recent local sample presented in Poznanski et al. (2009). The observed magnitude $m_x$ and statistical uncertainty $\sigma_{m_x}$ in each passband $x$ is taken from our plateau fit at day $t = t_{\text{exp}} + 50(1 + z)$, and is used to determine a realization of the observed-frame SDSS magnitudes at rest-frame day 50. The uncertainty in the redshift is also included in the Monte Carlo, but as we have host-galaxy redshifts for most of our SNe, this source of uncertainty is small enough to have no significant effect on our results. The rest-frame day 50 Bessell $BVRI$ magnitudes are then calculated for each iteration, from which we obtain the average magnitude in each passband and its uncertainty. Although we cannot directly compare magnitudes in the SDSS filters to any other currently existing SN II-P data set, we compute SDSS magnitudes (asinh magnitudes are used by the SDSS-SNS, but apart from Figures 1 and 2 we use log10 magnitudes throughout this paper) and present them alongside the Bessell magnitudes in Table 1, which represents the results for this section.

The uncertainty in the date of explosion does not significantly affect the determination of the day 50 magnitude in a SN II-P, since the plateau is modeled as a linear evolution and the uncertainty about the explosion date is symmetric. However, the same is not true for the uncertainty in the day 50 magnitude. The plateau class, as discussed in P09, is not well defined, and
the only other SNe II-P in the SCM literature that have been
into the SN magnitudes. In the first test, we attempt to reproduce
the size of the effect for each SN will vary.
plateau and the size of the explosion date uncertainty, and thus
magnitude uncertainties depend strongly on the slope of the
Deviation from a completely flat plateau, the more important
decline rate of SNe II-P can vary widely. The greater the
50 magnitudes at day 50. These two SNe do not pass our sample cuts (Section 2.1),
Notes. Magnitudes listed here are derived for 50 days after the explosion, and have been both K-corrected and corrected for MW extinction along the line of sight. Bessell BVRI magnitudes are calculated in the Vega system and have been S-corrected from the observed filters; SDSS gri magnitudes are standard log10 magnitudes (not asinh, as in Holtzman et al. 2008), and are in the AB system. We model the plateau as an exponential in flux space, and fold into our photoelectric corrections the uncertainties in observed flux, explosion epoch and redshift. The 21 SNe listed here include the 15 SCM sample SNe, as well as those that only fail our spectroscopy cut (described in Section 2.1).

| IAU Name | Redshift | B | V | R | I | g | r | i |
|---------|----------|---|---|---|---|---|---|---|
| 2007id  | 0.0270(0.0050) | 19.23(0.06) | 18.32(0.04) | 18.01(0.02) | 17.86(0.02) | 18.77(0.06) | 18.15(0.02) | 18.22(0.02) |
| 2006aw  | 0.0307(0.0055) | 19.82(0.02) | 18.97(0.01) | 18.56(0.01) | 18.31(0.01) | 19.39(0.01) | 18.74(0.01) | 18.65(0.01) |
| 2007ib  | 0.0330(0.0050) | 19.63(0.08) | 18.74(0.05) | 18.39(0.03) | 18.20(0.02) | 19.18(0.07) | 18.54(0.03) | 18.55(0.02) |
| 2007ji  | 0.0500(0.0050) | 20.79(0.06) | 19.90(0.04) | 19.55(0.03) | 19.37(0.04) | 20.34(0.05) | 19.71(0.03) | 19.73(0.03) |
| 2005gj  | 0.0505(0.0050) | 20.72(0.01) | 20.07(0.01) | 19.74(0.01) | 19.50(0.02) | 20.35(0.01) | 19.92(0.01) | 19.84(0.01) |
| 2007md  | 0.0546(0.0050) | 22.22(0.18) | 20.90(0.09) | 20.18(0.04) | 19.60(0.06) | 21.65(0.15) | 20.43(0.05) | 20.12(0.04) |
| 2006ji  | 0.0555(0.0050) | 20.50(0.03) | 19.65(0.02) | 19.32(0.01) | 19.10(0.04) | 20.06(0.02) | 19.48(0.01) | 19.48(0.02) |
| 2007lx  | 0.0568(0.0050) | 21.14(0.06) | 20.40(0.03) | 20.05(0.02) | 19.83(0.06) | 20.75(0.05) | 20.22(0.03) | 20.17(0.03) |
| 2007nw  | 0.0572(0.0050) | 21.65(0.10) | 20.63(0.04) | 20.26(0.03) | 19.92(0.10) | 21.16(0.08) | 20.42(0.04) | 20.40(0.06) |
| 2007kv  | 0.0602(0.0050) | 21.45(0.10) | 20.57(0.07) | 20.17(0.06) | 19.97(0.14) | 21.01(0.08) | 20.34(0.06) | 20.31(0.08) |
| 2007kx  | 0.0680(0.0050) | 21.24(0.06) | 20.28(0.03) | 19.86(0.02) | 19.57(0.03) | 20.77(0.05) | 20.04(0.02) | 19.98(0.02) |
| 2006gq  | 0.0698(0.0050) | 21.29(0.03) | 20.52(0.02) | 20.21(0.01) | 19.99(0.04) | 20.88(0.03) | 20.37(0.01) | 20.36(0.02) |
| 2007ky  | 0.0736(0.0050) | 22.05(0.07) | 21.01(0.03) | 20.56(0.02) | 20.22(0.06) | 21.55(0.06) | 20.74(0.02) | 20.66(0.03) |
| 2007lz  | 0.0940(0.0050) | 22.77(0.22) | 21.98(0.16) | 21.30(0.07) | 20.51(0.21) | 22.38(0.19) | 21.62(0.10) | 21.10(0.12) |
| 18321a  | 0.1041(0.0050) | 22.01(0.08) | 21.19(0.04) | 20.83(0.03) | 20.73(0.09) | 21.59(0.06) | 20.97(0.03) | 21.03(0.05) |
| 2006kn  | 0.1203(0.0050) | 22.45(0.13) | 21.53(0.08) | 21.03(0.06) | 20.97(0.33) | 22.02(0.10) | 21.19(0.07) | 21.21(0.16) |
| 2007kz  | 0.1274(0.0050) | 22.71(0.10) | 21.81(0.06) | 21.27(0.04) | 21.25(0.28) | 22.29(0.08) | 21.44(0.05) | 21.46(0.14) |
| 2007rw  | 0.1439(0.0050) | 22.68(0.25) | 22.05(0.16) | 21.68(0.17) | 22.31(0.14) | 22.79(0.21) | 21.77(0.17) | 22.24(0.55) |
| 2007nr  | 0.1444(0.0050) | 22.67(0.09) | 22.17(0.06) | 21.72(0.05) | 21.78(0.29) | 22.39(0.08) | 21.88(0.05) | 21.95(0.15) |
| 2007gy  | 0.1462(0.0050) | 23.15(0.34) | 22.07(0.17) | 21.90(0.22) | 21.19(0.84) | 22.57(0.23) | 22.09(0.22) | 21.96(0.45) |
| 2007nl  | 0.1683(0.0050) | 22.14(0.36) | 22.03(0.26) | 21.66(0.41) | 20.57(1.29) | 21.93(0.30) | 22.07(0.38) | 21.42(0.73) |

4. SPECTROSCOPIC ANALYSIS

The expansion velocity of the ejecta in SNe II-P is the key to the SCM, as it is this parameter that correlates with
luminosity; overluminous SNe have high expansion velocities and underluminous SNe have low velocities (HP02). The ejecta velocity is determined by measurements of the weak Fe ii absorption lines around \( \lambda \approx 5000 \) Å, in particular the Fe ii \( \lambda 5169 \) line (Hamuy 2003). Unfortunately, the velocity of this feature is often difficult to measure. Two methods have been explored in previous studies for extracting the Fe ii velocity in such a way that the measurement of the H\( \beta \) absorption feature, which is often stronger (particularly at early times) than the Fe ii absorption feature, that biases the cross-correlation fit; without masking the galaxy lines we derive the velocity from the Fe ii \( \lambda 5169 \) absorption feature, \( v_{\text{Fe ii}} \), before applying the SCM to this sample.

We list in Table 2 the velocities and statistical uncertainties derived using this method for each spectrum of a SN II-P in our SCM sample (shown in Figure 3). After computing the Fe ii velocity of each spectrum with the above technique, we extrapolate the velocity of the ejecta at \( t = 50 \) days using Equation (1) from N06,

\[
v_{\text{Fe ii}(50)} = v_{\text{Fe ii}(t)}(t/50)^{0.464 \pm 0.017}.
\] (1)

The range of epochs that this function, which is derived from fitting published velocities of SNe II-P with multi-epoch spectra, is claimed to be valid for is days 9–75 post-explosion. We only list in Table 2 spectra that fall in this range; we leave out our spectra that were taken at earlier epochs. The day 50 ejecta velocities for our SCM sample of SNe II-P are shown in Table 3. For those SNe that have multi-epoch spectra we have taken a weighted average of the velocity derived from each spectrum. The large uncertainties in velocity for some SNe are a result of either having only one spectrum at an early time, or having a larger uncertainty (\( >5 \) days) in the explosion epoch; for several SNe both conditions apply. The uncertainties in \( v_{\text{Fe ii}(50)} \) given in Table 3 do not include the effects of peculiar motion, which contributes an uncertainty in velocity of 300 km s\(^{-1} \). We add this uncertainty in quadrature to that in Table 3 when we use our data in the SCM.

5. STANDARDIZED CANDLE METHOD

The SCM assumes the magnitudes of SNe II-P are correlated with the velocity of the ejecta, as measured by the Fe ii \( \lambda 5169 \) absorption line. The observed magnitude in the rest-frame I band has been shown empirically to obey the relation

\[
m_I = M_{I_b} - 5 \log_{10}(v_{\text{Fe ii}(50)}/5000) + R_I[(V - I) - (V - I)_0] + 5 \log_{10}(D_L(z)\Omega_M, \Omega_\Lambda),
\] (2)

where the \( K \)-corrected apparent magnitude \( m_I \), color \( V - I \) absolute magnitude \( M_{I_b} \), and Fe ii velocity \( v_{\text{Fe ii}} \) (in units

\[\text{Table 2}\]

| IAU Name   | \( t - h^a \) (days) | \( v_{\text{Fe ii}} \) (km s\(^{-1} \)) | Observatory |
|------------|----------------------|--------------------------------------|-------------|
| 2007ld     | 11(5.5)              | 7860(720)                            | APO         |
| 2006iw     | 16(5.5)              | 7370(710)                            | NTT         |
| 2007ib     | 13(1.0)              | 7870(750)                            | NTT         |
| 2006jl     | 22(7.0)              | 5700(400)                            | Subaru      |
| 2007lj     | 59(7.0)              | 3870(430)                            | Subaru      |
| 2007lx     | 18(8.0)              | 6430(220)                            | Subaru      |
| 2007nw     | 20(7.0)              | 6730(440)                            | Subaru      |
| 2006kv     | 13(4.0)              | 7000(610)                            | APO         |
| 2007kw     | 19(2.5)              | 6350(670)                            | TNG         |
| 2006gq     | 14(3.0)              | 5680(580)                            | NTT         |
| 2007ky     | 17(3.0)              | 5990(590)                            | NTT         |
| 18321      | 26(5.0)              | 7170(630)                            | TNG         |
| 2006kn     | 19(1.5)              | 6970(700)                            | TNG         |
| 2007kz     | 18(3.5)              | 6660(400)                            | TNG         |
| 2007mr     | 39(5.0)              | 5290(370)                            | Subaru      |

Notes. Listed are all of the spectra taken between rest-frame days 9 and 75 after the explosion for our SCM sample; note the bias in observed epoch toward early times. The velocity of the Fe ii line and its uncertainty for each spectrum is obtained from the cross-correlation code of P09. Uncertainties in explosion epoch and observed-day velocity are given in parentheses.

\[\text{Table 3}\]

| IAU Name   | Redshift | \( v_{\text{Fe ii}} \) (km s\(^{-1} \)) | \( I \) | \( V - I \) |
|------------|----------|--------------------------------------|--------|-----------|
| 2007ld     | 0.0270   | 4105(574)                            | 17.86(0.02) | 0.46(0.04) |
| 2006iw     | 0.0307   | 4488(164)                            | 21.83(0.02) | 0.66(0.02) |
| 2007ib     | 0.0330   | 3945(337)                            | 18.20(0.02) | 0.58(0.05) |
| 2007lj     | 0.0500   | 4215(464)                            | 19.37(0.04) | 0.53(0.06) |
| 2006jl     | 0.0555   | 5560(313)                            | 19.10(0.04) | 0.55(0.04) |
| 2007lx     | 0.0568   | 3901(819)                            | 19.83(0.06) | 0.57(0.07) |
| 2007nw     | 0.0572   | 4287(754)                            | 19.92(0.10) | 0.71(0.11) |
| 2006kv     | 0.0620   | 3644(616)                            | 19.97(0.14) | 0.60(0.16) |
| 2006gq     | 0.0698   | 3404(149)                            | 19.99(0.04) | 0.53(0.04) |
| 2007ky     | 0.0736   | 3513(407)                            | 19.76(0.02) | 0.79(0.07) |
| 18321      | 0.1041   | 5056(636)                            | 20.73(0.09) | 0.46(0.10) |
| 2006kn     | 0.1203   | 4220(443)                            | 20.97(0.33) | 0.56(0.34) |
| 2007kz     | 0.1274   | 4307(322)                            | 21.25(0.28) | 0.56(0.29) |
| 2007mr     | 0.1244   | 4398(349)                            | 21.78(0.29) | 0.39(0.30) |

Notes. Derived SN parameters required for the SCM analysis. Magnitudes and velocities listed are for \( z = v + (1 + z) \), the derivation of these values are described in Section 3 and Section 4. Magnitudes have been K- and S-corrected, and corrected for Milky Way extinction. An additional uncertainty of \( r_{\text{pec}} = 300 \) km s\(^{-1} \) is added in quadrature to both the redshift \( z \) and the velocity derived from the Fe ii \( \lambda 5169 \) absorption feature, \( v_{\text{Fe ii}} \), before applying the SCM to this sample.
of km s$^{-1}$) are all measured at 50 days post explosion. We follow HP02, N06, and P09 in performing the standardization technique using the $I$-band magnitude. As in P09, we allow the extinction law $R_I \equiv A_I/E(V-I)$ to be a free parameter in our analysis, and adopt the ridge-line SN II-P color from N06, $(V-I)_0 = 0.53$ mag (the exact value of this color is not important, as the parameter is degenerate with $M_{I_0}$). Since we are measuring only relative distances, we use the “Hubble Constant free” absolute magnitude and luminosity distance, $M_{I_0} \equiv M_{I_0} - 5 \log_{10}(H_0) + 25$ and $D_L \equiv H_0 D_L$ (P09; Goobar & Perlmutter 1995; Sullivan et al. 2006). We assume throughout this paper a fiducial LCDM cosmology with $\Omega_M = 0.3$, since we are unable at these redshifts to put a meaningful constraint on cosmology. Though we fit for free absolute magnitude $M_I$, we are measuring only relative distances, we use the “Hubble Constant free” absolute magnitude and luminosity distance, $M_{I_0}$ throughout this paper, assuming $H_0 = 70$ km s$^{-1}$ Mpc$^{-1}$. This allows for a more intuitive understanding of the standard absolute magnitude of SNe II-P.

We find the best-fit values of our free parameters by running a Monte Carlo Markov Chain (MCMC) to minimize the negative log of the likelihood function with respect to the velocity term coefficient $\alpha$; the color law $R_I$; the “Hubble Constant free” absolute magnitude $M_{I_0}$; and the intrinsic dispersion $\sigma_{\text{int}}$. Correcting an error in Equation (4) of P09, we have

$$-2 \log(L) = \sum_{SN} \left\{ \frac{(m_I^{\text{obs}} - m_I(v_{Fe II}, V - I, z; M, \alpha, R_I))^2}{\sigma_{\text{total}}^2} + \log(\sigma_{\text{total}}^2) \right\},$$

(3)

where the summation is over all SNe in the sample; $m_I(v_{Fe II}, V - I, z; M, \alpha, R_I)$ is defined by Equation (2); and the total uncertainty is

$$\sigma_{\text{total}}^2 = \sigma_{m_I}^2 + \frac{\alpha}{\ln 10} \sigma_{v_{Fe II}}^2 + (R_I \sigma_{(V-I)})^2 + \left( \frac{5}{\ln 10} \sigma_{D_L(z)}^2 \right) + \sigma_{\text{int}}^2.$$

(4)

The logarithmic term in Equation (3) comes from the normalization of the likelihood function; this term weights against excessively large values of the free parameters, which could otherwise be favored by the first part of the log-likelihood function. The variable $\sigma_{\text{int}}$ represents the amount of intrinsic scatter among SNe II-P that cannot be accounted for by the model itself, and thus represents the minimum statistical uncertainty in any distance determination from the SCM.

In Table 3 we present the rest-frame magnitudes and velocities at day 50 for the 15 SNe II-P that comprise the SCM sample from the SDSS-SNS. When our SNe are added to the existing sample of SNe II-P with measurements at day 50 (presented in Table 2 of P09), the SCM can be applied over a nearly continuous redshift range, $0.001 < z < 0.25$.

6. RESULTS

Combining the 15 SDSS SNe II-P in Table 3 with the 34 SNe II-P in the “culled” set of P09, the best-fit SCM parameters as determined by minimizing Equation (3) are

$$M_I = -17.52 \pm 0.08, \alpha = 4.0 \pm 0.7, \text{ and } R_I = 0.8 \pm 0.3,$$

with an intrinsic dispersion $\sigma_{\text{int}} = 0.29$ mag. The Hubble diagram and the Hubble residuals of the combined data set is plotted in Figure 5. The scatter found here is comparable to the results of N06 and Olivares (2008), but the addition of the SDSS SNe increases the dispersion from the 0.22 mag found in P09.

To find the dispersion of SNe II-P from a true standard candle, we minimize Equation (3) while fixing the parameters $\alpha$ and $R_I$ to zero. HP02 quote an $I$-band dispersion without any corrections of 0.80 mag, and P09 state the dispersion of the “culled” sample to be $\approx 0.9$ mag. When we solve for the dispersion from a true standard candle of the P09 “culled” sample using our Equation (3), we find $\sigma_{\text{int}} = 0.67$ mag. The SDSS-only set of SNe II-P introduced here has a much smaller true intrinsic dispersion; $\sigma_{\text{int}} = 0.22$ mag. We show in Section 6.1 that this tight scatter can be attributed to selection effects.

Using the SCM reduces the intrinsic scatter in the SDSS SNe II-P from 0.22 to 0.16 mag, with best-fit parameters of $M_I = -17.67^{+0.10}_{-0.11}, \alpha = 1.8^{+0.9}_{-1.0}, \text{ and } R_I = 0.1 \pm 0.5$. These results are significantly different than the “culled” sample of 34 SNe in P09, whose parameters we calculate to be $M_I = -17.38 \pm 0.08, \alpha = 4.2 \pm 0.6, \text{ and } R_I = 0.8 \pm 0.3$. The SDSS SNe have a standard magnitude that is brighter than the pre-existing sample by $> 2\sigma$; have a weaker correlation with the velocity of the ejecta; and display no strong correlation between color and luminosity. Figure 6 projects the likelihood

![Figure 5](image-url)
surface of the two samples onto the $\alpha-M_{K_S}$ and $\alpha-R_I$ planes, showing that in the former these two samples do not intersect at the 2σ level. It is interesting to note that the high-redshift SNe of N06 also did not intersect with the low-redshift SNe of HP02 at the 2σ level in the $\alpha-M_{K_S}$ plane (see Figure 14 of N06).

We also note that the SCM parameters we give for the P09 “culled” set are not the same as the published values. These parameter differences exist because our Equations (3) and (4) are slightly different from what was used in P09. We stress that the differences we find are small; $\alpha$ is lower by 0.2, $R_I$ is unchanged, $M_I$ is 0.01 mag more luminous, and the intrinsic dispersion, 0.20 mag, is 0.02 smaller than in P09. The SCM parameters we list in Table 4 for various SNe II-P sample combinations and those stated throughout the remainder of the paper are, unless stated otherwise, calculated using the equations in Section 5.

In P09, the initial result for $\sigma_{int}$ with their full sample of 40 SNe II-P was 0.38 mag. The three SNe with the largest Hubble residuals (in units of standard deviations) in P09 all were found to have positive decline rates in the $I$ band between days 10 and 50 post-explosion. By removing all SNe from their sample that had a positive decline rate at the 1σ level, P09 obtained a value for $\sigma_{int}$ of only 0.22 mag. We calculate the intrinsic scatter of the “full” and “culled” sets in Table 4 to be 0.35 and 0.20 mag, respectively. In total, 6 of their 40 SNe, all of which came from the 19 SNe detected by KAIT, were eliminated with the decline rate cut.

To find the slope of the $I$-band light curve for every SDSS SN II-P, we $K$- and $S$-correct each observed epoch in the light curve of each SN; this process is described as method B in Section 3. We find that the rest-frame $I$-band light curve has a positive decline rate for 6 of our 15 SNe. Plotting decline rate against the distance of each SDSS SN II-P from the Hubble line derived from the SDSS-plus-P09 sample (in units of standard deviation), we find that none of the five most deviant SNe in our sample would be removed using the decline rate method. Therefore, we cannot use the culling method of P09 to identify a more standard subclass of SNe II-P. Whereas the inclusion of the SDSS SNe II-P substantially increases the intrinsic $I$-band dispersion of the “culled” P09 sample, the intrinsic dispersion of the full sample is unchanged by this addition.

We also comment here on the effect of peculiar velocity on our results. We state in Section 4 that for our SNe II-P sample we add in quadrature 300 km s$^{-1}$ to the uncertainty in $v_{pec}$ to account for the peculiar velocity of the SNe within its host galaxy. In P09, a smaller uncertainty is added to the expansion velocity of each SN, and this source of uncertainty is not mentioned at all in N06. If we change the uncertainty of each SN in the P09 “culled” and “full” sets to reflect a $\sigma_{v_{pec}}$ of 300 km s$^{-1}$, we find no significant difference in the best-fit SCM parameters of the combined data sets. The intrinsic scatter of the P09 SNe would be smaller if this peculiar velocity uncertainty were used, but the parameters again would remain relatively unchanged. Since our main conclusions are not affected by this source of uncertainty, we choose to adopt the $v_{pec}$ uncertainties as is from Table 2 of P09.

6.1. Selection Effects and Biases

The disparity between the SCM fit parameters from the SDSS SNe and those presented in P09 requires explanation. We take a close look at selection effects, as well as the techniques used to obtain the magnitudes and velocities in Table 3, for potential sources of bias that could cause our results to differ from previous works.

One possible explanation of the relatively high luminosity of our sample when compared with previous SNe II-P studies is selection effects (though selection effects may have affected the results of previous work as well, as mentioned in N06). To examine the effects of Malinqui bias, we calculate the absolute magnitudes of the SDSS SNe II-P assuming our fiducial cosmology. The narrow range of day 50 magnitudes we find, $-17.1 < M_I < -17.9$, conflicts with the well known fact that SNe II-P occupy a range of luminosities spanning at least two orders of magnitude (See Figure 7). Since the data presented here are a compilation of objects discovered by the SDSS-SNS during drift-scan searches, there is no expectation of completeness amongst the data, and a bias toward intrinsically brighter objects above some redshift is inevitable. We use the Supernova Analysis package (SNANA; Kessler et al. 2009b).
and perform an analysis similar to that in Dilday et al. (2008, 2009) to determine the probability of detecting a SN II-P of a given luminosity in the SDSS-SNS. We find that for a SN II-P with an absolute $r$-band magnitude of $-16.0$ in its plateau (absolute $I$-band magnitude of $-16.54$) located at a redshift of $0.07$ (apparent $r$-band magnitude of $21.63$), the detection efficiency by the SDSS-SNS is $\sim 75\%$. At a redshift of $0.054$, the probability of detection is $\sim 90\%$. This effect clearly explains why our SNe II-P sample does not contain any dim SNe above $z \approx 0.10$.

While Malmquist bias limits the magnitude distribution of our sample at higher redshift, it does not explain why we do not see intrinsically dimmer SNe at lower redshifts. However, not all supernova candidates discovered in the survey were observed spectroscopically, which is for obvious reasons a necessary condition for the SNe in our SCM sample. While candidates with a peak observed $r$-band magnitude of $\approx 20.5$ or brighter were spectroscopically followed up in all cases, dimmer candidates were subject to more selective criteria (Sako et al. 2008). Due to this brightness cutoff for spectroscopic observations, the aforementioned SN II-P with absolute $r$-band magnitude of $-16.0$ would be included in our SCM sample only at redshifts of $z < 0.043$. We also give priority to SNe that have good contrast with their host galaxy, which further biases against dimmer SNe. When these observational limitations are considered, the relatively high intrinsic luminosity of our SN II-P sample—and thus the small intrinsic scatter—can be understood as the result of a magnitude limited search compounded by spectroscopic selection effects.

The small intrinsic scatter in $I$-band magnitudes amongst our SNe II-P sample limits its utility for a self-contained determination of the velocity parameter $\alpha$. The smaller the range of absolute magnitudes in a sample, the smaller the range of Fe II velocities we expect to find. This effect is compounded by the relatively large uncertainties in our day 50 Fe II velocities; there are more SNe II-P with $\sigma_{v_{\text{Fe II}} > 400}$ km s$^{-1}$ in our sample of 15 SNe than in the entire P09 “culled” sample. This partially explains the loose constraints that the SDSS data set is able to put on $\alpha$; both the results of P09 and no velocity dependence are consistent with our marginalized $\alpha$ at $2\sigma$. However, this effect is not able to explain why the intrinsic scatter increases when we apply the SCM to the combined sample of SDSS-plus-P09 SNe II-P.

To determine if we see any effects of bias as a function of redshift within our sample, we split our data into two roughly equal in size high- and low-redshift samples (redshift cut at $z = 0.065$) and determine the best-fit SCM parameters for each. Although the resulting parameters have large uncertainties due to the low statistics, both sets of data have the same absolute magnitude and velocity parameters ($\alpha = 2.1 \pm 0.8$ and $1.9 \pm 1.1$ for low- and high-$z$, respectively). However, the value of the reddening term $R_I$ differs greatly; $R_I = 1.8 \pm 0.8$ for the low-$z$ sample, and $R_I = -0.4 \pm 0.4$ for the high-$z$ sample. We reanalyze the low-$z$ SNe by systematically removing one object at a time and re-computing the $R_I$ parameter, and find that the high value of the low-$z$ reddening law parameter can be attributed to SN 2006iw, which has the smallest uncertainty in day 50 $V-I$ color of any object in our SCM sample (see Table 3). The $R_I$ parameter is effectively unchanged if any other low-$z$ SN is removed in the re-sampling analysis, but is consistent with zero when we remove SN 2006iw. We find no evidence of bias in our fitted parameters as a function of redshift.

We examine the effects of host galaxy extinction. We expect to see fewer reddened objects at high redshifts; a given supernova appears brighter in a host galaxy with less extinction, and therefore is more likely to appear in our survey. We do not find a strong trend of color as a function of redshift in our sample. While our most distant SNe do have smaller $V-I$ values, the uncertainties are larger at these redshifts. One aspect of our selection criteria for spectroscopic observation was that the SN be easily separated from its host galaxy; in effect, this requirement biases us against having heavily extincted, low-$z$ SNe II-P in our sample. We also note that the colors of the SNe in our sample, though skewed toward the bluer end, fall within the range of observed values in P09. The distribution of SN colors we observe and the resulting reddening parameter we obtain are both well explained by selection effects.

It is reasonable to question whether selection effects that bias against fainter SNe being observed should even matter. After all, the SCM is the Standardized Candle Method; if a SN II-P sample consists of only bright SNe, these should all have high ejecta velocities, and therefore no bias should be introduced. So, while the intrinsic magnitude dispersion without any corrections would appear tighter—and the average absolute magnitude brighter—than expected from a non-biased sample, the SCM should correct for this bias. Malmquist bias alone is therefore unable to explain why we obtain a more luminous value of $M_b$ from the SDSS-SNS sample of SNe II-P than P09. However, bias can still affect the analysis in a secondary manner if the measurement of the standardizing parameter is biased for the most luminous objects. We examine whether the measurement of the ejecta velocity in our sample is biased toward lower values.

As previously mentioned, the similarity in the derived $\alpha$ parameter at both low and high redshifts suggests that such a secondary bias, if one exists, is not a function of redshift. Our spectra for high redshift SNe are primarily from larger telescopes, so the S/N of these spectra are not necessarily worse than those of low redshift SNe. The distribution of uncertainties in the day 50 Fe II velocities of the SDSS SNe II-P is flat as a function of redshift. We do not appear to be biased against measuring ejecta velocity with less precision at high redshift.
The distribution of day 50 ejecta velocities from our SN sample and the “culled” sample in P09, which were determined using the same method, is shown in Figure 8. The similarity of the distributions of these two data sets is difficult to reconcile with their different luminosity distributions within the context of the SCM. One explanation for the difference could be that our day 50 magnitude derivation is systematically too luminous; since we have already shown that we expect our sample to be biased toward more luminous SNe, and the photometry for our sample is of excellent quality, this explanation seems unlikely (though we return to K-correction uncertainty later). Another explanation of this effect could be that the measurement of our day 50 velocity is systematically offset to lower values. Using the observed values of the I-band magnitudes and V − I colors from our sample of SN and assuming the SCM parameters from the “culled” sample of P09, we calculate the expected value of the day 50 Fe ii velocity for each SDSS SN II-P and compare it with our derived values. The observed velocity is lower than that predicted by the P09 parameters by an average of ~1300 km s$^{-1}$; only 3 of the 15 SNe are within 1σ of the predicted velocity. We examine whether the low velocities of our bright sample could be caused by the N06 velocity extrapolation or the P09 cross-correlation method.

Equation (1) relates the velocity of the ejecta at any epoch from day 9–75 to that at day 50, in the middle of the plateau. The distribution of epochs that we have spectra for is heavily skewed toward pre-day 50; only one SN in this study had a spectrum taken after day 50, and only a few had any taken post day 30. If the relationship between the velocity at early times and day 50 is not accurately represented by Equation (1), we could be biasing our results relative to P09 and N06, which primarily have spectra from later epochs. There are only three SNe in our sample for which we have one spectrum taken before day 20 and one at or after day 30, and in each one of these cases the extrapolated day 50 velocity from the earlier spectrum is lower than that derived from the later spectrum. This would seem to imply that the epoch of the observation can bias the resulting day 50 Fe ii velocity. However, there is no spectrum at any epoch in our data set that has an Fe ii velocity high enough to match the prediction from the P09 set of parameters for the day 50 ejecta velocity of that SN; this suggests that our results cannot simply be ascribed to a bias in the N06 fitting function. Furthermore, we applied Equation (1) to each of the Fe ii velocities quoted in Quimby et al. (2007) for the very well observed Type II-P SN 2006bp, and found that for this object the direction of bias is reversed; the day 50 velocity obtained using the Fe ii velocities for the three spectra at $t < 20$ days is higher by 1000 km s$^{-1}$ than that obtained from each of the four velocity measurements at $t > 30$ days. The accuracy of using Equation (1) is therefore difficult to establish, as the velocity of the ejecta at early times may not have a one-to-one relationship with the velocity at day 50.

The cross-correlation method of P09 for deriving the Fe ii velocity from a SN II-P spectrum (D. Poznanski 2009, private communication) is applied in this paper to all of our SNe, as this should allow the most consistent comparison with the velocities derived for the full “culled” sample of P09. However, as our spectra are typically from earlier epochs than in P09, it is possible that the cross-correlation is systematically underestimating the velocity at these times, leading to our low ejecta velocities. We test for an early epoch bias by running the cross-correlation code on the SN 2006bp spectra obtained from the SUSPECT database, and compare the resulting velocities with those derived in Quimby et al. (2007) from the minima of the features in the Fourier transform-smoothed spectra. There are two important aspects to our results. First, the P09 method returns a much lower velocity for each epoch than is quoted in Quimby et al. (2007), and the difference between the two methods is a strong function of epoch: the P09 method differs by 300–400 km s$^{-1}$ at $t ≥ 25$ days, while it is slower by at least 1500 km s$^{-1}$ at $t < 20$ days. This difference between methods reinforces the notion that it is very difficult to measure accurately the velocity of a wide absorption feature, particularly at early epochs. However, since this method is used to measure velocities uniformly across data sets, the offset from the values of Quimby et al. (2007) should not be of importance to this work. Second, using the velocities derived from the cross-correlation method, we find that the spectra at days 16 and 21 predict a higher day 50 Fe ii velocity for SN 2006bp than the day 42 and 57 spectra by ~600 km s$^{-1}$; the early spectra overpredict the ejecta velocity in the plateau. Another potential source of bias comes from the fact that early spectra are often dominated by Hβ in the 4500–5500 Å range, so the cross-correlation could be matching this feature instead of Fe ii $λ$5169. Since Hβ is found at higher velocities than Fe ii $λ$5169, though, this effect could not result in our velocities being biased to lower values. We thus find no indication that our velocities have been systematically offset to lower values due to the application of Equation (1) or the P09 cross-correlation method. Since introducing a different method of calculating the Fe ii velocities from our spectra is likely to provide biased results with respect to the data presented in P09 (as shown with SN 2006bp), we retain these two techniques as our spectroscopic analysis.

The final source of uncertainty in our data is due to spectral templates. As mentioned earlier, the SNe we observe are at high enough redshifts for K-corrections to be necessary, and we must perform S-corrections as well to place our data in the same filters as observed in previous studies. These corrections require knowing the spectral energy distribution of each SN at the epoch (in our case, 50 days post explosion) we wish to correct—which we do not have. Thus, we must use a spectral template, which, though we warp the template to match observed colors, may not account for all variations between different SNe, and will be a source of error with unknown magnitude. We are unable...
to create a template from our own data, as our spectroscopic follow-up program was biased toward early times, resulting in only one spectrum beyond day 40. We use throughout this paper the same spectral template that was adopted for $K$-corrections in N06. To test the extent to which warping the template can account for spectral differences between SNe, we obtained from the SUSPECT database a day 51 spectrum of SN 2004et and a day 42 spectrum of SN 2006bp. Neither of these spectra cover the entire range of wavelengths necessary to perform our warp and $K$-corrections (3500–11000 Å), so we scaled and pasted the N06 template to the blue and red end of each spectrum. When we calculate the $I$-band magnitudes for the SDSS SNe II-P using these new spectral templates, we find an average systematic uncertainty of 0.03 mag. It is possible that with a larger database of spectra containing more diversity, we might find larger systematic uncertainties through the same test. However, $I$-band $K$-corrections using the spectrum of SN 2004et are 0.2 mag larger than the $K$-corrections using the N06 template and SN 2006bp when we do not warp the template. The fact that the systematic uncertainty after warping is much smaller demonstrates that the act of warping the spectrum to the observed colors can correct for the majority of intrinsic dispersion amongst spectral templates.

7. DISCUSSION

We have presented photometric and spectroscopic data for 15 SNe II-P from the SDSS-II Supernova Survey. These SNe span a range of redshifts not covered by other surveys, connecting the local sample of HP02 and P09 to the high-$\alpha$ range of redshifts not covered by other surveys, connecting SNe II-P from the SDSS-II Supernova Survey. These SNe have faster ejecta, at primary relationship defining the SCM, which is that brighter SNe II-P to constrain the SCM parameters, we observe the velocity determination. Despite the selection effects and sources of systematic uncertainty in our analysis. The low $\alpha$ value we derive for the SDSS-only sample is due to both the small scatter in observed magnitudes and the uncertainty in our velocity determination. Despite the selection effects and measurement uncertainties that limit the power of the SDSS SNe II-P to constrain the SCM parameters, we observe the primary relationship defining the SCM, which is that brighter SNe have faster ejecta, at $\approx 2\sigma$.

The primary objective of the SDSS-II Supernova Survey was to identify and characterize SNe Ia; as a result, the observing strategy was not ideal for SNe II-P studies. A future survey program that would focus on the SCM would greatly benefit from possessing the following qualities:

1. Longer continuous survey duration. For the final six weeks of such a survey, any newly discovered SNe will not have photometry sufficiently far into their plateau to allow extrapolation of their magnitudes at rest-frame day 50. In addition, no SN can have its explosion date pinned down unless it happens after the first survey observation in its field. Since each season of the SDSS-II SNS was three months long, no more than 50% of the survey time was useful for discovering new SNe II-P. Doubling the length of such a survey would nearly triple the number of SNe discovered for which the SCM can be used.

2. Deeper, later spectroscopic observations. When a new SN is discovered in a survey dedicated to SNe II-P, an initial quick spectrum is not needed. A SN II-P will have a distinct light curve from a SN Ia, and thus valuable spectroscopic resources will not be used to follow up objects of no interest. Since the velocity of the ejecta at day 50 is what is required, a spectrum at early times is not required, and observations can target day 50. As we have shown, the systematic uncertainties associated with early-time spectra require a thorough study. Also, each object must be observed for a sufficient time to obtain a high quality S/N spectrum. Accurate measurements of Fe $\text{II} \lambda 5169$ absorption lines are key to determining the strength of the $\alpha$ parameter; quality over quantity should be the mantra for these followups.

3. Template database must be extended. To perform both $K$-corrections and $S$-corrections, an accurate representation of the true spectral energy distribution is vital. Ideally, the spectrum for each SN in such a survey would have sufficient wavelength coverage to allow corrections for all bands of interest to be computed from it directly. As this situation is unlikely, complementary spectral observations that cover the near IR should allow for templates to be constructed that range from at least 4000–12000 Å (or redder still, if the wavelengths in the lowest energy filter are redshifted out of this range at the targeted $\alpha$). The amount of uncertainty in the day 50 magnitude results that is due to relying on a limited number of SNe II-P spectral templates will only be known when more extensive templates are available.

When these advances can be made, we will be able to determine whether the SCM and SNe II-P can place meaningful, independent constraints on cosmological parameters.

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