Comparative studies of low temperature X-ray diffraction experiments on $R_2\text{Ir}_2\text{O}_7$ ($R = \text{Nd, Eu, and Pr}$)

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(Dated: June 25, 2014)

The cubic symmetry of pyrochlore iridium oxides $R_2\text{Ir}_2\text{O}_7$ ($R = \text{Nd, Eu, and Pr}$) has been investigated by high resolution X-ray diffraction experiments down to 4 K, in order to clarify the relationship between the metal-insulator transition (MIT) and the small structural phase transition suggested by Raman scattering experiments in these compounds. We have found that a small negative thermal expansion of the order of $10^{-3}$ Å appears only in Nd$_2$Ir$_2$O$_7$ below the MIT, $T_{\text{MIT}} = 34$ K, resulting in the magnetovolume effect of the long-range order of Ir moments. However, any breaking of the cubic symmetry of three iridates has not been observed as appearance of superlattice reflections nor splittings of cubic reflections below $T_{\text{MIT}}$. These results imply that lowering of the cubic symmetry plays a minor role for the change in the electronic state of these compounds, while a formation of the special arrangement of Ir moments plays a major role for the MIT.

PACS numbers: 73.10.+h, 61.05.cf, 75.47.-m, 72.80.Ga

I. INTRODUCTION

Geometrically frustrated magnets with metallic conduction have attracted much attention because of the realization of a new type of electronic and magnetic behavior, originating from the interplay between frustrated spins and conduction electrons. The pyrochlore iridates $R_2\text{Ir}_2\text{O}_7$ ($R = \text{Y, Pr–Lu}$) are one of the candidates to study such a correlated state, where an unconventional anomalous Hall effect, giant magnetoresistance, heavy Fermion behavior, and metal-insulator transition (MIT) have been observed. Band calculations indicate that in the metallic phase the conduction band near the Fermi level consists of Ir 5d and O 2p orbitals, while in the insulating phase Ir ions are expected to be tetravalent (Ir$^{4+}$, 5d$^5$) and the significance of the strong spin orbit interaction and electron correlation inherent to the Ir element, which can lead to exotic electronic and magnetic phases, including a topological Mott insulator, a Weyl semimetal, and an axion insulator.

Experimentally, most of $R_2\text{Ir}_2\text{O}_7$ compounds exhibit MIT in accordance with magnetic phase transitions. Recent studies on systematic replacement of $R$ ions indicated that the transition temperature of the MIT, $T_{\text{MIT}}$, decreases with increasing the ion radius of rare earth ions. Interestingly, it is found that the system becomes metallic in the vicinity of $R = \text{Nd}$ and Pr, where the long-range magnetic order is also suppressed and the spin-liquid like phase is suggested. Mechanical pressure experiments also indicated an anomalous metallic phase which can appear in the suppression of the MIT.

Stimulating these experimental results and recent extensive attention to an exotic electronic phase for 5d transition metal systems, several experimental investigations on $R_2\text{Ir}_2\text{O}_7$ compounds have also been performed to clarify the origin of the MIT. Raman scattering experiments focused on a relationship between the MIT and the crystal-structure phase transition which has been often observed in 3d transition metal oxides. The results for sintered powder samples of $R = \text{Sm, Eu}$ and a single crystal of Nd showed that an additional development of a Raman peak, a signature of the structure phase transition, was observed below $T_{\text{MIT}}$ for Sm$_2$Ir$_2$O$_7$ and Eu$_2$Ir$_2$O$_7$, while no clear signals appear for Nd$_2$Ir$_2$O$_7$. More recent resonant X-ray diffraction (XRD) experiments on a single crystal of Eu$_2$Ir$_2$O$_7$, however, did not observe the crystal-structure phase transition, although the experiments clarified the long-range order of Ir$^{4+}$ moments consisting of an all-in all-out magnetic structure. Neutron diffraction experiments also suggested the long-range order of Ir moments in Nd$_2$Ir$_2$O$_7$, where the all-in all-out structure of the ordered moments was also expected. Therefore, in the magnetic point of view, something electronic correlation with relating to the ordering of Ir moments, rather instead of relating to the crystal-structure phase transition and its effect to the band structure, is essential for the MIT of $R_2\text{Ir}_2\text{O}_7$, as in the case of Cd$_2$Os$_2$O$_7$. A recent theory has also suggested that a purely electronic mechanism is sufficient, examining a finite temperature effect for physical properties. However, the situation is still complicated because of the discrepancy of experimental results for the crystal structure, and of the possible effect of the structural change with the lattice distortion. It is thus essential to clarify the low-temperature crystal structure as well as the possible emergence of the crystal-structure phase transition in these compounds.

In this study, we have performed low-temperature and high-resolution X-ray diffraction experiments on powder samples of Nd$_2$Ir$_2$O$_7$ (NIO), Eu$_2$Ir$_2$O$_7$ (EIO), and Pr$_2$Ir$_2$O$_7$ (PIO). We focused on the previous experimental results of Raman scattering and expected that the change in the crystal-structure phase transition is very
small even though there exists the phase transition. We thus used a high resolution X-ray diffractometer which can detect a change of the lattice parameter of the order of $10^{-4}$ Å ($\Delta \theta \sim 0.001^\circ$)\textsuperscript{38}. We have measured temperature dependence of the lattice parameter very precisely down to 4 K and found a negative thermal expansion that appears only for NIO at temperatures below $T_{\text{MIT}} = 34$ K. The crystal structure retains the cubic pyrochlore structure (space group $Fd\bar{3}m$, No.227) for all three compounds down to 4 K. These results suggest that the crystal-structure phase transition from the cubic pyrochlore structure is not the main origin of the MIT. Instead, a formation of the special arrangement of Ir$^{4+}$ magnetic moments could lead to a crucial effect for the emergence of the MIT of pyrochlore iridates, which should also affect the magnetovolume effect of these compounds.

II. EXPERIMENTAL

Polycrystalline samples of NIO, EIO and PIO were prepared by a standard solid-state reaction\textsuperscript{2,10,39}. The appropriate amounts of Nd$_2$O$_3$ (99.99%, Rare Metallic Co., Ltd.), Eu$_2$O$_3$ (99.99%, Rare Metallic Co., Ltd.) or Pr$_9$O$_{11}$ (99.99%, Rare Metallic Co., Ltd.) and IrO$_2$ (> 99.9%, Tanaka Kikinzoku Kogyo K. K.) were mixed for 30–60 minutes and pressed into pellets. The pellets were wrapped with Pt foils and placed in evacuated quartz tubes. These products were then heated at 1173 K for about 3 days. After this reaction, additional 3% of IrO$_2$ was added. The pellets of the mixtures, wrapped with Pt foils, were heated again at 1473 K for about 10 days in evacuated quartz tubes. In this process, several intermediate grindings were performed in order to react the samples well.

X-ray powder-diffraction experiments were carried out using a Rigaku SmartLab powder diffractometer equipped with a Cu K\textsubscript{\alpha} monochromator. The sample was mounted in a closed-cycle He-gas refrigerator and the temperature was controlled from 300 to 4 K. Details of the confirmation of the sample quality are described in a later section.

To check physical properties of obtained powder samples, the specific heat ($C_P$) and dc magnetic susceptibility ($M/H$) were measured with a commercial calorimeter (Quantum Design, PPMS) and with a SQUID magnetometer (Quantum Design, MPMS). The electrical resistivity $\rho$ was also measured by using a standard four-probe method for rectangular samples cut out from pellets.

III. RESULTS

Before going to low temperature XRD experiments, we have checked the sample quality at room temperature (RT). Figure 1 shows the diffraction patterns and the results of Rietveld refinement by using RIETAN-FP\textsuperscript{40}. We confirmed that XRD patterns of NIO, EIO, and PIO were reasonably fitted by parameters of the cubic pyrochlore structure with the space group $Fd\bar{3}m$. The refined structure parameters are listed in Table I. The final $R$ factors of the refinements are $R_{wp} = 7.16\%$, $R_e = 5.88\%$, and $R_p = 5.31\%$ for NIO, $R_{wp} = 4.54\%$, $R_e = 3.57\%$, and $R_p = 3.31\%$ for EIO, and $R_{wp} = 8.68\%$, $R_e = 5.90\%$, and $R_p = 6.39\%$ for PIO, respectively. The goodness-of-fit parameter, $S = R_{wp}/R_e$, was $S = 1.21, 1.27$, and 1.47 for NIO, EIO, and PIO, respectively, indicating that the qualities of the fitting are good. Note that we confirmed a few amount (< 1%) of an impurity phase such as Nd$_{9.33}$(SiO$_4$)$_6$O$_2$ in our samples, however it does not affect the peak profiles and intensities of main peaks such as (440), (444), and (800) for the low-temperature XRD experiments and physical properties. We thus considered...
TABLE I: Structure parameters at RT for the powder samples of $R_2$Ir$_2$O$_7$ ($R = \text{Nd, Eu, and Pr}$) of Fig. 4 refined by Rietveld analysis. The analysis was performed assuming the space group $Fd\bar{3}m$ (No. 227). The lattice constant $a$ is obtained as $a = 10.3768(2) \, \AA$ for Nd$_2$Ir$_2$O$_7$, $a = 10.2857(3) \, \AA$ for Eu$_2$Ir$_2$O$_7$, and $a = 10.4105(3) \, \AA$ for Pr$_2$Ir$_2$O$_7$, respectively. The $U_{iso}$ parameter of 16c(Ir) of Nd$_2$Ir$_2$O$_7$ and Pr$_2$Ir$_2$O$_7$ was fixed in the analysis. $U_{iso}$ values of 48f(O) and 8b(O) of three compounds were also fixed in the analysis.

| Atom | Site | x  | y  | z  | $U_{iso}$ ($10^{-3} \, \AA^2$) |
|------|------|----|----|----|-----------------|
| Nd   | 16d  | 1/2| 1/2| 1/2| 1.3(1)          |
| Ir   | 16c  | 0  | 0  | 0  | 1.7(1)          |
| O    | 48f  | 0.330(1) | 1/8 | 1/8 | 5 (fix) |
| O'   | 8b   | 3/8| 3/8| 3/8| 5 (fix)        |
| Eu   | 16d  | 1/2| 1/2| 1/2| 4.2(2)          |
| Ir   | 16c  | 0  | 0  | 0  | 1.7(1)          |
| O    | 48f  | 0.336(1) | 1/8 | 1/8 | 5 (fix) |
| O'   | 8b   | 3/8| 3/8| 3/8| 5 (fix)        |
| Pr   | 16d  | 1/2| 1/2| 1/2| 1.9(1)          |
| Ir   | 16c  | 0  | 0  | 0  | 1.7(1)          |
| O    | 48f  | 0.330(1) | 1/8 | 1/8 | 5 (fix) |
| O'   | 8b   | 3/8| 3/8| 3/8| 5 (fix)        |

that our powder samples were reasonable for the experiments.

The prepared samples exhibit qualitatively the same behaviors of $M/\mathcal{H}$, $C_P$, and $\rho$ as those of the previous reports.\cite{9,11,39} We confirmed that the second-order phase transition of the MIT appear at $T_{MIT} = 34 \, \text{K}$ for NIO and at $T_{MIT} = 120 \, \text{K}$ for EIO (Fig. 2). For PIO, the metallic behavior was confirmed down to 2 K of the present lowest measured temperature, where PIO does not show any signatures of a magnetic phase transition and MIT. It can thus be considered that PIO becomes a reference compound for NIO and EIO when comparing behaviors with and without the MIT. Note that the absolute value of $\rho$ of PIO is slightly larger than that of Ref. [10], while it is almost the same as that of Ref. [33]. This result is probably due to the grain boundaries in the pelletized samples, which brings about a weak localization of conduction electrons. It is also noted here that a slight discrepancy between our sample and previous polycrystalline samples\cite{9,39} was observed in the $T$-dependence of $\rho$ for EIO below $T_{MIT}$. This result may come from the effect of a small amount of the off-stoichiometry of samples.\cite{39} We will discuss it in a later section.

Next, we have checked the possibility of a crystal-structure phase transition for NIO and EIO. We did not observe an additional developing of peak intensity, as well as splitting or broadening of certain peaks in the XRD patterns at temperatures below $T_{MIT}$: i.e., $T_{MIT} = 34 \, \text{K}$ for NIO and $T_{MIT} = 120 \, \text{K}$ for EIO. Even though there exists an emergence of extra peaks, peak intensities are expected to be below 0.01% of the maximum peak counts of the (111) peak, where $2 \times 10^5 \sim 1 \times 10^6$ counts were integrated in our experiments. It is thus considered that the crystal symmetry retains the cubic pyrochlore structure even for a low temperature phase of NIO and of EIO. In Fig. 3, we show representative peak profiles around the (444) peaks of NIO and EIO, respectively. One can see no splitting and broadening of the peaks below $T_{MIT}$. In these experiments, the peak positions are determined within a very small experimental error of 0.001°, as in the case of previous experiments on the powder sample of Tb$_2$Ti$_2$O$_{19.5}$.

We found a different temperature dependence of the lattice parameter for EIO and NIO. EIO shows a positive thermal expansion, while NIO shows a negative thermal expansion on warming. It is slight but experimentally clear for the peak shift of those compounds [insets of Figs. 3(a) and (b)], where the peak of EIO and of NIO goes forward and backward around $T_{MIT}$, respectively. In Fig. 4, we show the temperature dependence of the lattice parameter $a(T)$ of NIO and EIO, estimated from the peak position of the (444) peak at each temperature. The data was normalized by one at $T = 80 \, \text{K}$, $\Delta a(T)/a(80 \, \text{K})$, where $\Delta a(T) = a(T) - a(80 \, \text{K})$. For reference, we also show the results of PIO in the same experimental way. One can see that $\Delta a(T)/a(80 \, \text{K})$ continuously decreases on cooling for three compounds. However, only NIO exhibits the negative thermal expansion below $T_{MIT} = 34 \, \text{K}$. The same tendency was also confirmed by using other experimental results for converting $a(T)$ from peak positions of e.g. the (800) and (440) peaks for NIO [Fig. 4(b)]. The linear coefficient of the thermal expansion $\alpha = (1/\rho(T))(\partial \rho(T)/\partial T)$ is obtained as $\alpha = -1.5(1) \times 10^{-6} \, \text{K}^{-1}$ at $T = 35 \, \text{K}$ and $\alpha = 1.7(1) \times 10^{-6} \, \text{K}^{-1}$ at $T = 40 \, \text{K}$ for NIO. We can thus estimate the discontinuity of $\alpha$ around $T_{MIT}$ as $\Delta \alpha = -3.2(1) \times 10^{-6} \, \text{K}^{-1}$. Note that a very small up-
turn is also found at temperatures below 20 K for EIO and PIO, however the value of the changes is one order of magnitude smaller than that for NIO. In the whole measured temperature range, the full width at half maximum (FWHM) of profile peaks is almost \( T \)-independent (inset of Fig. 4 for the (444) peak), implying again no reduction of the crystal symmetry below \( T_{\text{MIT}} \) within the experimental accuracy.

It is worth noting here that we didn’t observe any obvious anomaly in \( \Delta a(T)/a(80 \text{ K}) \) at about \( T = 15 \text{ K} \) for NIO, where the localized moments of \( \text{Nd}^{3+} \) are known to exhibit an antiferromagnetic long-range order.\(^{33,35} \)

**IV. DISCUSSION**

From our low temperature XRD data presented above, we experimentally revealed that pyrochlore iridates of NIO and EIO do not show the crystal-structure phase transition at temperatures lower than \( T_{\text{MIT}} \). Moreover, within the experimental accuracy, the lattice distortion is almost isotropic [Fig. 3b)]. Therefore, we can conclude that the crystal-structure phase transition as well as the local and anisotropic lattice distortions in the cubic pyrochlore structure are not the main origin of the MIT of pyrochlore iridates in real materials. In contrast, our powder samples of NIO and EIO show the MIT and the magnetic anomaly in \( M/H \) at almost the same temperature, implying the long-range order of the \( \text{Ir}^{4+} \) moments forming the all-in all-out magnetic structure.\(^{33,35} \)

It is thus considered that the magnetic order with the special arrangement of Ir moments is attributable to the change in the electronic state at \( T_{\text{MIT}} \). A similar case has been recently pointed out for \( \text{Cd}_{2}\text{Os}_{2}\text{O}_{7} \).\(^{36} \) On the basis of the irreducible representation of the all-in all-out magnetic structure at the 16c-site atom of the pyrochlore lattice,\(^{36} \) the cubic structural symmetry can be preserved at temperatures above and below the magnetic phase transition. It is consistent with the present experimental results.

The incompatible behavior of the lattice expansion of NIO and of EIO can be understood semi-quantitatively by the Ehrenfest relation for a second-order phase transition: i.e., \( (\partial T_{\text{MIT}}/\partial P)_{\rho\to0} = T_{\text{MIT}} V_{\text{mol}} \Delta a / \Delta C_{\rho} \), where \( V_{\text{mol}} \) is the molar volume and \( \Delta C_{\rho} \) is the peak height of the specific heat at \( T_{\text{MIT}} \). From present \( C_{\rho} \) and XRD experiments and previous pressure-effect experiments,\(^{26,27} \) these values are roughly estimated as \( (\partial T_{\text{MIT}}/\partial P)_{\rho\to0} \approx -10 \text{ K/GPa, } \Delta C_{\rho} / T_{\text{MIT}} \approx 0.06 \text{ J/K}^2\text{mol, and } V_{\text{mol}} \approx 84 \text{ cm}^3/\text{mol at } T_{\text{MIT}} = \)
34 K for NIO, while \( \frac{\partial T_{MIT}}{\partial P} \bigg|_{P=0} \approx -5 \text{ K/} \text{GPa} \), 
\( \Delta C_P / T_{MIT} \approx 0.07 \text{ J/} \text{K}^2 \text{-mol} \), and \( \nu_{\text{mol}} \approx 82 \text{ cm}^3/\text{mol} \) at \( T_{MIT} = 120 \text{ K} \) for EIO, respectively. Therefore, the expected value of \( \Delta \alpha \) due to the phase transition can be calculated as \( \Delta \alpha_{\text{cal}} \approx -7 \times 10^{-6} \text{ K}^{-1} \) for NIO and \( \Delta \alpha_{\text{cal}} \approx -4 \times 10^{-6} \text{ K}^{-1} \) for EIO, respectively. Both compounds are expected to show the negative thermal expansion, however the change in NIO should appear as a larger effect at \( T_{MIT} \). In our experiments, it was estimated that \( \Delta \alpha = -3.2 \times 10^{-6} \text{ K}^{-1} \) for NIO. The absolute value of the experiment is somewhat smaller than that of the rough estimation above, although the order of the value is the same. We thus think that other extra effects could reduce the absolute value of the negative thermal expansion from the expected value for EIO as well. In any case, in view of the thermodynamic property of a phase transition, the negative thermal expansion observed in NIO can be understood in terms of the magnetovolume effect resulting in the magnetic phase transition of the Ir moments at about \( T_{MIT} \).

We finally comment on the discrepancy of the previous results about the crystal structure and electrical resistivity. One of the possible origins of these results may be attributed to the sample dependence. It is known that frustrated magnets often exhibit strong sample dependence due to the frustration among spin interactions and many-body effects. This tendency has also been found in pyrochlore oxides \( A_2B_2O_7 \) (\( A = \text{rare earth ions,} \ B = \text{transition metal ions} \)), including NIO, EIO, and PIO, as well as AIO, where the distribution of nonstoichiometric concentrations such as \( x \) and \( y \) of \( A_{2+x}B_{2-x}O_{7+y} \) is thought to induce sample dependent physical properties. Even in our samples, we also observed a slight discrepancy in EIO for the previous results. For examples, the upturn of \( \rho \) of EIO below \( T_{MIT} \) is suppressed in our samples, as compared with the previous result in Ref. [10]; however, it should be noted here that in contrast to both results, the sample of EIO in Ref. [8] retains the metallic behavior without an any signature of the MIT. Recent studies on single crystalline samples of EIO showed that \( \rho \) is quite sensitive to the off-stoichiometry \( x \) of samples. According to this result, \( x \approx 0.02 \) is expected for the previous polycrystalline sample of EIO in Ref. [10], while \( x \approx 0.03 \) for our samples. Such a small distribution (\( \approx 1\% \) discrepancy) gives rise to a strong sample dependent physical property in these compounds. Therefore, we should take care of the sample quality for studying the frustrated pyrochlore magnets, although this problem could be a signature of exotic materials. In the present experiments, we used identical batch samples for experiments of \( C_P, M/H, \) and \( \rho \) as well as the low-\( T \) XRD experiments. We thus consider that present experimental results provide compatible and consistent data for the discussion about the relationship between the MIT and the structural phase transition in pyrochlore iridates, i.e., large structural changes do not occur even when the MIT is visible in the materials.

V. CONCLUSION

We have performed the high-resolution and low-temperature X-ray diffraction experiments on polycrystalline samples of \( R_2Ir_2O_7 \) (\( R = \text{Nd, Eu, and Pr} \)), in order to clarify the relationship between the MIT and the crystal-structure phase transition. We confirmed that the structure symmetry of these compounds is not broken, preserving the cubic pyrochlore lattice symmetry even below the transition temperature of the MIT: \( T_{MIT} = 34 \text{ K} \) for \( \text{Nd}_2Ir_2O_7 \) and \( T_{MIT} = 120 \text{ K} \) for \( \text{Eu}_2Ir_2O_7 \). We also found the positive thermal expansion for \( \text{Eu}_2Ir_2O_7 \) and \( \text{Pr}_2Ir_2O_7 \), while the negative thermal expansion for \( \text{Nd}_2Ir_2O_7 \), which may come from the magnetovolume effect resulting in the long-range order of Ir magnetic moments. These results suggest that the crystal-structure phase transition from the cubic pyrochlore structure, analogously to the case of 3d transition metal oxides, is not the origin of the MIT of NIO and EIO. Instead, the results imply that the formation of the special arrangement of Ir moments should affect the change in the electronic state of these compounds at \( T_{MIT} \). Experimental studies using high-quality single crystals are important for further clarification of the origin of the MIT in pyrochlore iridates.

Acknowledgment

This work was partly supported by Grant-in-Aid for Young Scientists (B) (Grant No. 24740240) from the Ministry of Education, Culture, Sports, Science and Technology.

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