An Unexpected Cubic Symmetry in Group IV Alloys Prepared Using Pressure and Temperature

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Abstract: The cubic diamond (Fd3m) group IVA element Si has been the material driver of the electronics industry since its inception. We report synthesis of a new cubic (Im3m) group IVA material, a GeSn solid solution, upon heating Ge and Sn at pressures from 13 to 28 GPa using double-sided diamond anvil laser-heating and large volume press methods. Both methods were coupled with in situ angle dispersive X-ray diffraction characterization. The new material substantially enriches the seminal group IVA alloy materials landscape by introducing an eightfold coordinated cubic symmetry, which markedly expands on the conventional tetrahedrally coordinated cubic one. This cubic solid solution is formed, despite Ge never adopting the Im3m symmetry, melting inhibiting subsequent Im3m formation and reactant Ge and Sn having unlike crystal structures and atomic radii at all these pressures. This is hence achieved without adherence to conventional formation criteria and routes to synthesis. This advance creates fertile avenues for new materials development.

Introduction

Despite the overwhelming importance of cubic diamond Si in electronic applications, its indirect band-gap and fixed lattice constant make it considerably less effective for optoelectronic applications.[1] While solid solution with isostructural Ge facilitates tunability of both lattice constant and band-gap, the SiGe band-gaps remain indirect.[2,3] Conversely, alloying Ge with Sn can provide tunability and direct band-gap formation making this one of the most actively investigated systems for optoelectronic applications.[4–7] These investigations are mostly confined to thin films because Ge and Sn are immiscible in the bulk at ambient pressure.[8,9] Change in miscibility and bulk synthesis can however be achieved using high pressure and temperature to access regions of the phase diagram where Ge and Sn become similar enough.[10] Between ambient pressure and 10 GPa Ge adopts a cubic structure with Fd3m symmetry whereas Sn adopts a tetragonal structure with I4/amd symmetry (β-Sn). At 10 GPa cubic Ge also transforms to the tetragonal structure with I4/amd symmetry (β-Ge). Sn on other hand, transforms above 10 GPa to another tetragonal structure with I4/mmm symmetry (t-Sn).[11] β- and t- throughout always designate the I4/amd and I4/mmm space groups, respectively. The only pressure where Ge and Sn can be similar enough according to the Hume-Rothery criteria,[12] is at 10 GPa. In particular, based on the consideration that at 10 GPa Ge and Sn could uniquely adopt the same tetragonal crystal structure with I4/amd symmetry and have atomic radii ratios below the Hume-Rothery 15% tolerance threshold, we heated Ge and Sn at this pressure and indeed recovered a bulk GeSn solid solution with P4,2,2 symmetry.[10,13] However, several further heating experiments above this a priori unique pressure, at between 11–24 GPa also led to recovery of bulk GeSn solid solutions, frequently nanocrystalline[14] with the cubic diamond structure, containing up to 30 at% Sn. This surprising result indicated that reaction between Ge and Sn was occurring with facility in an extended pressure regime, where it was considered unfavourable.

Results

To investigate this high pressure region for potential existence of a hidden alloy structure, we performed numerous experiments using both laser-heated diamond anvil cell and scale-up multianvil methods, both of which were coupled with

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We present examples from both types of... time quenching. The left and right horizontal bars are not scales, but references to correlate times on the right vertical axis with their corresponding temperatures on the left vertical axis.

![Figure 1](image)

Figure 1. a) Angle-dispersive X-ray diffraction patterns upon heating and melting of a β-Ge and t-Sn mixture at 15.9 GPa in a multi-anvil device and formation of a bcc structure with Im3m symmetry (a = 3.481(1) Å) at 777 K (Figure S6, Le Bail fitting in the supporting information) before melting. b) Upon re-crystallization a structure with a nominal “Im3m” symmetry exhibits significant anisotropy and diffraction intensity variation. Indexing of this structure is consistent with the Im/mmm symmetry with a/c = 0.97 \(a = 3.552(1)\) Å, c = 3.430(1) Å (top pattern) (Figure S7, Le Bail fitting in the supporting information) which is not far from cubic. This phase, with this c/a ratio, is stable down to 4.2 GPa with exsolution of β-Sn beginning below 10 GPa (Figures S8–12, Le Bail fitting in the supporting information). (c) Time-temperature-intensity-two-theta plot at 15.9 GPa through melting and upon annealing on re-solidification and then temperature quenching. The left and right horizontal bars are not scales, but references to correlate times on the right vertical axis with their corresponding temperatures on the left vertical axis.

We present examples from both types of experiments. The first example is from one of our multianvil studies where a 60:40 at% β-Ge and t-Sn mixture was heated at 15.9 GPa, then melted, followed by temperature quenching and decompression to ambient pressure (Figure 1). As seen in Figures 1a, c, upon heating at 15.9 GPa, the diffraction patterns of both t-Sn and β-Ge decrease in intensity. Interdiffusion between the two elements begins at about 400 K. Indeed between 298 and 548 K the leftmost t-Sn peak shifts from 5.038 to 5.057 degrees unlike the case upon heating pure t-Sn where it shifts like all other t-Sn peaks to the left due to thermal expansion. Shift to the right here means diffusion of Ge into Sn. At 756 K, the diffraction patterns of the starting phase structures have almost disappeared and three distinct diffraction peaks emerge which are indexed to the bcc structure with Im3m symmetry (Figure 1a). The values of parameter a adjacent to individual peaks in the figures were evaluated for each of these peaks by assuming that the peaks belong to the Im3m phase (see also section 6 supplementary information). If the a’s evaluated do not substantially differ from each other (< 0.015 Å) and from the lattice parameter evaluated from Le Bail whole pattern fitting, then this supports the cubic assignment and concomitant absence of significant anisotropy. If the pattern is not cubic the parameters will likely differ significantly and cannot be fit to cubic using Le Bail. Upon further heating, the diffraction pattern of Im3m strengthens while residual other sample peaks largely vanish. At 777 K whole pattern fitting (Le Bail method) provides a lattice parameter of 3.481 Å for the new phase (Figure 1a, Figure S6). At 828 K the new phase melts. The only diffraction peaks remaining at this temperature are the broad MgO peaks of the encapsulating octahedron (Figure 1a, c). Upon cooling, only the first two diffraction peaks re-emerge, as measured at 674 K and at 298 K. These could only nominally be indexed to a distorted Im3m symmetry because the lattice parameters calculated from each of these peaks, differ now by more than 0.06 Å (Figure 1b,c, Figure S7). This is unlike the case before melting where virtually no anisotropy is present and unlike the experiments with no melting, where no anisotropy is observed at any stage based on the fitting of individual peaks, the Le Bail whole pattern fittings and space group Im3m assignments documented in section 6 in the supporting information. Upon decompression in this experiment (Figure 1b), this distorted Im3m phase, whose diffraction peaks also exhibit significant intensity variations, is preserved down to 4.2 GPa (Figures S7–12). However below 10 GPa, Sn diffuses out of the structure, as seen by the emergence of β-Sn below this pressure. On recovery, Im3m and nanocrystalline Fd3m Ge-Sn alloys are obtained (Figure S3). A multianvil experiment with the same starting composition as above but without melting is shown in Figure 2. The pattern evolution is very similar to that of the previous experiment upon heating (Figure 2a,c, Figure S13). However in contrast to the previous experiment, upon temperature quenching no notable anisotropy or diffraction intensity variation is observed in the quenched Im3m phase (Figure 2b, top two
patterns, Figures S14,15). Below 10 GPa, Sn and Ge-rich alloys with \( \text{I}_4/\text{amd} \) symmetry emerge (bottom two patterns, Figures S16,17). On recovery, Ge-Sn alloys with \( \text{I}_4/\text{amd} \) and \( \text{P}4_2\text{~2} \) symmetries, as well as Ge with \( \text{P}6_3/\text{mmc} \) symmetry are obtained (Figure S4).\(^{10,11,15-17}\)

We also present an example from our double-sided laser-heated diamond anvil cell experiments on synthesis of this new cubic alloy (Figure 3). A nominal 60:40 at % \( \beta \)-Ge and t-Sn mixture in a neon pressure medium was heated at 21 GPa.\(^{28}\) As in the multianvil experiments described above, as the temperature was raised, the diffraction peaks associated with the endmember Ge and Sn phases weakened and largely vanished and were replaced by a diffraction pattern containing only the new \( \text{I}_3\text{~m} \) phase together with neon diffraction peaks (Figure 3a, Figure S18).\(^{15}\) Upon decompression (Figure 3b) the new cubic phase is still observed at 11 GPa, whereas below 10 GPa the GeSn \( \text{I}_3\text{~m} \) phase disproportionates into Sn-rich and Ge-rich tetragonal phases with \( \text{I}_4/\text{amd} \) symmetry (Figure S19–22).\(^{15}\) On recovery in this experiment, pure Ge with \( \text{I}3\text{~} \) symmetry, Sn-rich \( \text{I}_4/\text{amd} \) and Ge-rich \( \text{Fd}3\text{~m} \) were observed (Figure S5).\(^{15,19,20}\) An example of a synthesized \( \text{I}_3\text{~m} \) phase from a nominal 60:40 at % \( \beta \)-Ge and t-Sn starting mixture, using an argon pressure medium,\(^{24}\) at 21 GPa after quenching, is also shown in Figure 4 (Figure S23).\(^{15}\)

**Discussion**

With the unexpected formation of this new cubic phase established, we now consider the several unusual aspects associated with this synthesis. The first is the atomic radii incompatibility of endmember Ge and Sn for solid solution formation. The endmembers \( \beta \)-Ge and t-Sn with their different crystal structures also have atomic radii which markedly differ from each other by about 18% throughout the 13 to 28 GPa synthesis regime.\(^{15,16,22}\) Despite this incompatibility and operation well outside the apparent singular compatibility “sweet spot” of 10 GPa, cubic solid solutions with \( \text{I}_3\text{~m} \) symmetry were prepared throughout the 13–28 GPa regime (Figures 1–4).\(^{15}\) The explanation for this, is that the atomic radii within the coordination polyhedra of the endmember structures are not the appropriate compatibility manometer here. It is instead, the radii that the elements will adopt in the coordination polyhedra of the new structure. Ge in \( \beta \)-Ge is coordinated to 4\(+2\) nearest neighbours.\(^{11}\) In the cubic structure with \( \text{I}_3\text{~m} \) symmetry however, Ge is coordinated to 8 nearest neighbours.\(^{11}\) An expression introduced by Pauling\(^{23}\) allows us to estimate a Ge radius in eightfold coordination resulting in a radius expansion of about 15% from that in sixfold coordination.\(^{15}\) Sn only starts forming this cubic structure above 40 GPa and completely above 70 GPa,\(^{24}\) but its radii in our lower pressure regime of synthesis can be evaluated through extrapolation from these higher pressures. With Ge and Sn both in 8-fold coordination, atomic radii ratios are estimated to be within 2% of each other, so well within the Hume-Rothery compatibility boundary of 15%.\(^{12,15}\) (Figure S2).

This however highlights the second unusual aspect of this synthesis. \( \text{I}_3\text{~m} \) Sn only exists as a single phase above 70 GPa. Our results show however, that incorporation of Ge in Sn lowers the formation pressure of a pure \( \text{I}_3\text{~m} \) phase by...
a striking 50 GPa. This dramatic lowering of Im$\bar{3}$m stabilization pressure cannot be attributed to chemical pressure alone because the radius of Ge in the cubic structure with Im$\bar{3}$m symmetry is very similar to that of Sn. Ge promoting Im$\bar{3}$m formation is moreover, counter-intuitive because Ge, for very specific reasons presented below, does not form the Im$\bar{3}$m phase at any pressure. Therefore, Ge should hinder, not enhance formation of the Im$\bar{3}$m phase. In Ge namely, the s and p states are sufficiently close in energy that sp$^3$ hybridization and the associated tetrahedrally coordinated diamond structure, are favoured. With increasing pressure, sp$^3$ hybridization only gradually becomes less favourable in Ge with respect to promotion of electrons from the s-state to the p-state. The ensuing higher pressure intermediate bonded and distant from cubic Ge structures with Im$\bar{3}$m symmetry are dictated by this s-p favourability interplay and the diamond structure. This channeling away from the bcc (Im$\bar{3}$m) structure for Ge (and Si) is terminated one row down in the group IVA column, with Sn, because in Sn, the s and p states are no longer very close in energy. Thus the s-p electron promotion cost does not exceed that gained from sp$^3$ hybridization. Therefore the adoption upon compression of higher coordinated structures and the bcc symmetry in pure Sn are governed by the domination of de-hybridized p-electron states over sp hybridized ones. However entropy can
have a significant stabilization effect on alloys,[26,27] and incorporation of Ge will contribute favourably in this regard. This stabilizing effect will be further strengthened with increasing temperature through TΔS in the Gibbs free energy expression. Hence we put forth, that in the solid solution of Sn with Ge, together with still prevalently occupied p-electron states due to Sn, an energetically dominant entropic contribution through Ge incorporation contributes to the profound lowering of the formation pressure of the bcc (Im3m) phase. Indeed, entropic stabilization of otherwise unstable systems has been demonstrated, in other binary systems.[34]

A third unusual aspect is that melting is disruptive to the synthesis. Conventionally, melting is integral to synthesis as a part of a standard protocol in facilitating homogenization and more efficient reaction between starting materials, resulting in higher quality reaction products. Here, however, the opposite is true. We documented namely that melting is detrimental to formation of the isotropic cubic structure (c/a = 1) with Im3m symmetry (Figure 1) even with post-melt annealing, or even in other experiments, to complete inability to temperature-quench the new cubic phase, even if it had fully formed before melting. In sharp contrast, solely subliquidus annealing, where phase formation is governed by solid state diffusion is vital for high quality Im3m crystal development (Figures 1–4). An explanation for this is because the Sn liquid structure is considerably more anisotropic than the underlying Sn crystal structure, at the same pressure.[28,29] This is because a significant (50%), highly anisotropic β-Sn structural component (c/a = 0.54), is present in the liquid state even at 20 GPa, whereas in the solid state, β-Sn I4/amd (c/a = 0.54) completely transforms to t-Sn (c/a = 0.9) at 10 GPa.[19,28] Hence on melting, templating to highly anisotropic local β-Sn units hinders quenching of the new (c/a = 1) phase, in sharp contrast to interdiffusion upon heating in the solid state where the structural environment is considerably less anisotropic. Solid state reaction is also assisted by the low activation barrier for diffusion of Sn, where noticeable diffusion already starts as low as 391 K.[19] By employing solid state reaction exclusively, not only is the quality of the synthesized crystals much better, but the Im3m alloy could be recovered to room temperature at lower pressures than when attempting to quench after melting, even with post-melt annealing.

A fourth unusual attribute of this synthesis is that the specific volumes of t-Sn, β-Ge and our new cubic Im3m solid solution, indicate that not more than about 15 at % Ge should dissolve into Sn.[19] However the evolution of diffraction patterns in both the multi-anvil and the diamond anvil experiments reveal upon solid state heating, the emergence and strengthening of the Im3m solid solution pattern with a gradual decline of the other sample patterns until the Im3m solid solution pattern dominates (Figures 1–4). The explanation towards this is the marked influence that temperature has on the relative specific volumes of the reactants and products. For example, just below the melting temperature of Sn at a given pressure, Im3m solution with up to 46 at % Ge becomes favourable.[19] However the 60:40 starting Ge:Sn mix employed would still require a temperature exceeding the melting temperatures of the two components for complete incorporation. Also at the temperatures employed in the multi-anvil experiments, solution of up to about 24 at % Ge in Sn is favourable. Because Sn ex-solves on decomposition, the compositions during decomposition and upon recovery are not those of the new cubic phase, even though, they are often Ge-rich.

**Conclusion**

These results are also a fountainhead for exploring and exploiting new materials landscapes that include semimetals, post-transition metals as well as semiconductors, for both technological and fundamental benefit.[30] Here, we are completing in situ experiments on a binary solid solution formed at 10 GPa, which serves as the structural and electronic bridge between the known cubic Fd3m regime and the new cubic Im3m regime. Together with its crystal chemical importance we will exploit this “sweet spot” solid solution using its known composition as a single phase synthetic vehicle, to pinpoint the composition of our cubic Im3m solid solutions. We have also recovered a range of binary structures, including tetragonal P4_2_2, hexagonal P6_3mmc, cubic Ia3 and nanocrystalline cubic Fd3m phases with optoelectronic potential, that we are currently investigating. Moreover, configurational entropy, plays an important role in stabilizing the cubic Im3m solid solution. Hence we are also expanding the compositional range of the new cubic phase by introducing further components,[31] silicon in the first instance, which can also provide increased optoelectronic tunability. Additionally, we are using high pressure and temperature synthesis in conjunction with low temperature decompression as an additional avenue for stabilizing the new phase on recovery. The emergence of this previously hidden group IVA alloy structure is thus itself a source for further enrichment, of what is arguably the most technologically important column of the periodic table.

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**Conflict of interest**

The authors declare no conflict of interest.
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