The January 7, 2015, superbolide over Romania and structural diversity of meter-sized asteroids

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Abstract
Superbolides, i.e. extremely bright meteors produced by entries of meter-sized bodies into terrestrial atmosphere, are rare events. We present here detailed analysis of a superbolide, which occurred over Romania on January 7, 2015. The trajectory, velocity, and orbit were determined using two all-sky photographs from a station of the European Fireball Network (EN) in Slovakia and five casual video records from Romania, which were carefully calibrated. Bolide light curve was measured by EN radiometers. We found that the entry speed was 27.76 ± 0.19 km s⁻¹, significantly lower than reported by US Government sensors. The orbit was asteroidal with low inclination and aphelion inside Jupiter’s orbit. The atmospheric behavior was, however, not typical for an asteroidal body. The peak brightness of absolute magnitude of −21 was reached at a quite large height of 42.8 km and the brightness then decreased quickly. The bolide almost disappeared at a height of 38.7 km, leaving just a stationary luminous trail visible for several seconds. Only one small fragment continued until the height of 36 km. Brief meteorite searches were unsuccessful. The modeling of the light curve revealed that the body of initial mass of about 4500 kg remained almost intact until the dynamic pressure reached 0.9 MPa but it was then quickly disintegrated into many tiny fragments and dust under 1–3 MPa. A comparison was made with three other superbolides for which we have radiometric light curves: ordinary chondrite fall Košice, carbonaceous chondrite fall Maribo, and cometary Taurid bolide of October 31, 2015. The Romanian superbolide was not similar to any of these and represents probably a new type of material with intrinsic strength of about 1 MPa.

Keywords: meteor, meteoroid, asteroid, atmospheric entry

1. Introduction
Superbolides are extremely bright meteors, brighter in maximum than absolute (i.e. as seen from the distance of 100 km) visual magnitude of −17 (Ceplecha et al., 1999). Although bolide brightness depends on many parameters, e.g. meteoroid size, structure, and composition, entry speed and entry angle, we can roughly say that superbolides are caused by meteoroids of the sizes of the order of one meter and larger. In fact, meter-sized bodies are now often called asteroids rather than meteoroids (Borovička, 2016a). Regardless the terminology, bodies of these sizes belong to the least known objects in the Solar System. Current astronomical telescopes are sensitive enough to detect them when passing within few hundreds of thousands kilometers from the Earth, nevertheless, rarely is more information obtained than the orbit. Even the size is only approximate if albedo is not known. Properties, and in particular internal structure, of small asteroids are, nevertheless, of great interest from several reasons. Rotational rates of asteroids larger than about 200 meters (and smaller than about 10 km) suggest that large majority of them are weakly bound gravitational aggregates, so called rubble piles (e.g. Pravec and Harris, 2000). Smaller asteroids rotate generally much faster and can be monolithic, although it was suggested that many of them may be rubble piles as well, bound together by small van der Waals forces (Sanchez and Scheeres, 2014). Clarifying the question if small asteroids are monolithic or aggregates would shed light to the impact processes, in which these bodies are born. But even monolithic materials can have various structures and strengths, depending on the presence of cracks and other failures. Finally, even pristine Solar System materials have significant diversity as evidenced by meteorites, ranging from hard pure metals to
relatively soft carbonaceous bodies. Although meteorites are our best source of knowledge about microscopic and small-scale properties of asteroidal material, they are telling only part of the story. First, meteorites represent only the strongest parts of the original meteoroid or asteroid – the part, which was able to survive the atmospheric flight. Second, there are certainly meter-sized objects that are so weak that they do not drop any meteorites. An example was the body which produced the Šumava superbolide [Borovička and Spurný 1996].

The structure of small asteroids is of interest not only from purely scientific reasons. There are ideas of future retrieval and exploitation of small asteroids (e.g. [Hasnain et al.] 2012). The knowledge of physical properties of the target asteroid would be certainly crucial for the success of such an attempt. Small asteroids also pose non-negligible hazard when they enter the Earth’s atmosphere. The hazard was demonstrated by the crater producing Carancas impact (Borovička and Spurný 2008; Tancredi et al. 2009) and by the damaging blast wave produced by the Chelyabinsk entry (Brown et al. 2013; Popova et al. 2013). The actual effects on the ground caused by each particular entry depend to large extent on the internal structure of the impactor.

Observations of superbolides can, in fact, most easily provide information about the structure of meter-sized asteroids. Superbolides, however, are extremely rare events when observed from one site or from a limited region. [Ceplecha 1994] compiled 13 bolides from decades long observations by three fireball networks (plus one satellite tracked bolide), which he believed were all produced by bodies larger than 1 meter. He classified them according to the PE criterion developed earlier for smaller bolides (Ceplecha and McCrosky 1976) and based on bolide end height. Five of the 14 bodies were classified as soft cometary (the weakest known material). The remaining ones were mostly classified as carbonaceous. These results were not confirmed by the recent study of [Brown et al. 2016], which was based mostly on data from the US Government sensors obtained on global scale. The available data about 47 superbolides included only the location, height of maximum, velocity vector, and total radiated energy. Only one event had very high maximum (59 km), suggesting its cometary nature. The others had maxima at wide range of heights, 19 – 45 km, without obvious grouping. While those penetrating deeply were likely compact stones or metals, the nature of most bodies is not possible to judge from the data. They may have been fractured objects or bodies composed from weaker (e.g. carbonaceous) material.

[Popova et al. 2011] compiled data on 13 instrumentally observed meteorite falls. They were able to compare the atmospheric behavior with the properties of the recovered meteorites. More detailed observational data enabled the authors to find individual fragmentation points along the bolide trajectories. For all ordinary chondrites, the inferred strength of the incoming body was found to be one to two orders of magnitude lower than the meteorite tensile strength, presumably as a result of their collisional history. Low strength of some carbonaceous bodies may result, on the other hand, from their porous structures, more than fractures. The study of [Popova et al. 2011] was restricted to meteorite dropping events (of all sizes) and the study of [Brown et al. 2016] was based on very limited amount of data for individual events. Here we take advantage of good observational data we collected on the superbolide which occurred over Romania on January 7, 2015. It was a very bright event caused by a meter-sized asteroid but did not drop meteorites (at least none was found.
and none larger than a few grams could be expected). In addition to photographic and video records we have also obtained detailed radiometric light curves and we could model the atmospheric behavior of the body. The results could be compared with the modeling of three other superbolides of similar brightness, one ordinary chondrite, one carbonaceous chondrite, and one cometary body. The January 7, 2015, superbolide was also among those observed by the US Government sensors and we can compare our trajectory and orbital data with those reported by Brown et al. (2016).

2. Description of the event and available data

The superbolide studied here occurred over central Romania on January 7, 2015, 1:06 UT (3:06 local time). Despite the late night time, the bolide caused wide attention in the country, including news media. A number of videos, mostly from security cameras, showing intense illumination of the ground lasting for about two seconds were published on the Internet. Note that bright Moon (two days after the full Moon) was present high on the sky; the bolide was, nevertheless, much brighter. Several video cameras, including some cameras in neighboring countries Moldova and Serbia, captured the bolide itself. Sonic booms were reported in the region located about 100 km north of Bucharest.

The superbolide was also photographed by two all-sky cameras of the European Fireball Network (EN) located at Stará Lesná in Slovakia. Although the bolide was more than 600 km distant from there, it was well visible close to the horizon. Figure 1 shows part of the image from the Digital Autonomous Fireball Observatory (DAFO). DAFO contains two Canon EOS 6D digital cameras equipped with Sigma 8mm F3.5 EX DG Circular Fisheye lens. The exposure was 35 seconds long and sensitivity ISO 3200 was used. The camera contains a LCD shutter alternating between the open and close states with the frequency of 16 Hz. Due to the high brightness and low angular speed of the bolide, the breaks caused by the shutter are difficult to see. Nevertheless, the breaks were measurable on the original image (taken in the raw CR2 format) along part of the trajectory.

The second image from Stará Lesná (Fig. 2) was taken by an older device, the Autonomous Fireball Observatory (AFO), which was run simultaneously with DAFO. AFO uses photographic film Ilford FP125 and

| Name            | Longitude   | Latitude   | Altitude |
|-----------------|-------------|------------|----------|
| Sibiu           | 24.14375    | 45.78272   | 439      |
| Vojslobeni      | 25.63943    | 46.65971   | 825      |
| Eforie Sud      | 28.65293    | 44.01984   | 38       |
| Cluj-Napoca     | 23.61148    | 46.78548   | 340      |
| Gornovita       | 22.96138    | 45.06754   | 266      |
| Stará Lesná AR | 20.28823    | 49.15234   | 820      |
| Lysá hora       | 18.44764    | 49.54641   | 1324     |
| Červená hora    | 17.54196    | 49.77726   | 750      |
| Veselí n. M.    | 17.36962    | 48.95412   | 176      |
| Fierbinti       | 26.35945    | 44.67641   | 75       |

V – video, A – all-sky camera, R – radiometer, U – uncalibrated video

Table 1: Locations of various instruments used in this study

Figure 3: Light curve of the January 7 bolide in linear scale as taken by four independent radiometers. The differences in signal are caused by differences in sensitivity and range to the bolide. The noise is about 20 units, i.e. smaller than the width of the lines).

Figure 4: Map showing the location of used instruments relatively to the ground projection of the bolide trajectory. Filled circles are calibrated videos, empty circle is uncalibrated video, empty squares are photographic all-sky fireball cameras and crosses are radiometers (Stará Lesná provided two all-sky images and radiometric records).
Table 2: Parameters of videos and their calibrations

| Name          | Res x:y     | x:y       | Nter | Ncel | σ   |
|---------------|-------------|-----------|------|------|-----|
| Sibiu         | 586 × 480   | 0.9167    | 25   | 3    | 0.12|
| Voslobeni     | 800 × 480   | 1.25      | 35   | 0    | 0.25|
| Eforie Sud    | 704 × 576   | 0.9167    | 37   | 0    | 0.10|
| Cluj-Napoca   | 1280 × 960  | 1.00      | 36   | 0    | 0.034|
| Gornovita     | 704 × 576   | 0.9167    | 0    | 18   | 0.06|

Res – resolution in pixels, x:y – pixel scale ratio, Nter - number of terrestrial objects used for calibration, Ncel – number of celestial object measurements used for calibration, σ – formal uncertainty of coordinate calibration (degrees)

The 30mm fish-eye lens Zeiss Distagon F3.5 (Spurný et al., 2007). The sensitivity is lower and shorter part of the bolide was recorded by this camera. On the other hand, the brightest part was not so heavily saturated and shutter breaks could be measured, though with difficulties, along the whole recorded trajectory. Here the shutter was mechanical with the frequency of 15 Hz.

Both DAFO and AFO are also equipped with radiometers. Both radiometers are of the same type and are based on photomultiplier tube directed to zenith without any optics. The radiometers recorded total brightness of the sky during the bolide event with data frequency of 5000 Hz. The radiometers at even more distant stations of the EN recorded the superbolide as well. Figure 3 shows four independent radiometric curves. It can be seen that all features on the light curve are well reproduced on all curves.

Radiometers also provide exact timing based on the GPS PPS signal. We therefore know that bolide maximum occurred at 01:05:58.793 UT (the light travel time 0.002 s to Stará Lesná was taken into account).

The bolide was also photographed by a DAFO at Lysá hora, Czech Republic, but only small part of the trajectory was captured before the bolide crossed local horizon.

To compute bolide trajectory and velocity we had to use also casual videos from Romania. Casual videos need stellar calibration in order to obtain a reliable coordinate system. Nocturnal calibration images for 4 videos were taken between January 13 and February 3, 2015. The procedure described in Borovička (2014) was used for the calibration. All videos were taken by security cameras with known locations. In two cases (Sibiu and Eforie Sud) it was not possible to put the calibration camera exactly at the position of the security camera. The difference in position was therefore measured and appropriate correction was applied (Borovička, 2014). One additional video camera (in Gornovita) was calibrated using images of the Moon and Jupiter recorded directly by the video camera at var-
ious times. Table 1 lists the locations of all instruments used for the study of the bolide. It includes also another video from Fierbinti, which was taken by a dashboard camera in a moving car and could not be calibrated. This video, nevertheless, has the highest resolution (1920 × 1080 pixels, 30 frames per second) and shows most details about the bolide. All locations are also plotted at the map in Fig. 4. The videos are provided as supplementary files to the electronic version of this paper.

Table 2 summarizes the parameters of the videos and their calibration, namely the resolution in pixels, the pixel x:y size ratio (with one exception, the pixels were not squares), number of terrestrial objects used for calibration, number of celestial object measurements used for calibration, and the standard deviation of measurement in one coordinate. Note that the stellar calibration images involved between 156 and 577 stars and the standard deviations were between 0.009 and 0.015 degrees.

Except Cluj-Napoca, all video had relatively low resolution. The horizontal field of view was about 110° in all cases. All videos contained 25 frames per second. Selected frames from the Cluj-Napoca video are shown in Fig. 5. The first available frame (Fig. 5a) shows the bolide in flight. Since the camera recording was activated by the bolide motion when the bolide became sufficiently bright, the previous part of the flight was not recorded. While the bolide path at the edge of the field of view is well defined by the luminous trail, the velocity data are missing for this phase. In fact, positions of the bolide as a function of time could be measured only on frames 1–12. Later on, the bolide became too bright and so many pixels were saturated that positional measurement was not possible. After the maximum, only decaying luminous trail was visible for 2.5 seconds (Fig. 5e–f). The trail was useful for measuring bolide trajectory even during the brightest phase.

Figure 6 shows video frames from other four calibrated cameras. The bolide beginning is missing in all videos. In Gornovita, the record started only when the bolide became bright, similarly to Cluj-Napoca. In the remaining three cases the bolide beginning was out of the field of view. In Eforie Sud the bolide was already too bright to be measured when it entered the field of view. Only the trail position could be measured and no velocity data are therefore available from Eforie Sud. In Sibiu the camera wobbled in the wind. Fortunately, there were only two alternative positions and the wobbling could be therefore easily accounted for.

It was favorable that the brightest part of the trail exhibited, shortly before it disappeared, similar appearance in all videos. Four bright spots were resolved on four videos (except Gornovita, where the bolide was angularly short from geometric reasons). They are shown in Fig. 7. These spots were likely present at positions where large amount of dust was deposited. They were useful for checking the correctness of trajectory computations. If the trajectory solution is correct, the height of each spot in the atmosphere must be the same when computed from different cameras.

3. Trajectory

Bolide trajectory was computed by the straight least-squares method of Borovička (1990) using the azimuths and elevations of the bolide and the trail on the available videos and photographs. The method assumes that
Figure 8: Deviations of all individual positional measurements from the bolide trajectory. The miss distance of the lines of sight are given as a function of length along the trajectory (counted from the first measurement). Data from different cameras are given as different symbols. In the inset, the measurements of four bright spots shown in Fig. 7 are given. Here different symbols represent different spots.

the bolide trajectory is a straight line in the atmosphere, which was a very good approximation in this case (trajectories of long, nearly horizontally flying bolides may be curved by gravity). The trajectory is found by minimizing the miss distances (in km) of the individual lines of sight from the trajectory. Different weights can be given to measurements from different cameras depending on the quality of the camera and geometric factors such as distance to the bolide and bolide angular length as seen from the camera site. Bolide azimuths and zenith distances as measured from individual records are provided in the supplementary file coordinates.txt.

We succeeded to calibrate all data correctly, which is demonstrated in Fig. 8. All measurements are scattered along the trajectory with no systematic deviations and lie within 500 m of the trajectory, including data from 630 km distant Stará Lesná and 740 km distant Lysá hora. Only Voslobeni data show a small systematic trend. The calibration of this video was the worst (see Table 2) and the video therefore got a lower weight 0.1. The same weight was assigned to the Stará Lesná AFO. Lysá hora, with only five measurements along a small section of the trajectory, got a negligible weight 0.01. All other cameras had the weight 1.

An independent check of the trajectory solution is the position of four bright spots on the trail. Of course, since the video resolution is limited, there is some scat-
videos, was 38.7 km. This is the lowest point of the freshly visible trail. Due to the enormous brightness of the bolide in its final phase, the position of the bolide itself could not be measured. Neither could the bolide end be measured on the Stará Lesná digital photograph, where it is also heavily overexposed. There is, nevertheless, a small fragment visible in four frames of the uncalibrated Fierbinti video (Fig. 2). At the time when the lowest part of the trail was still very bright and saturated, the fragment emerged from the glow and moved further down. Since the same bright spots in the trail were visible (at a later time) here as on the other videos, the approximate bolide-height scale could be determined on the Fierbinti video as well. It follows that the fragment was observed at heights 37–36 km. It was also clearly visible that fragment velocity was decreasing.

4. Velocity and orbit

Bolide initial velocity was determined from the measurements of bolide positions on individual video frames and from the shutter breaks on Stará Lesná photographs. Each position can be converted into the length along the trajectory and length as a function of relative time is therefore obtained. Moreover, the digital photograph contains a time mark (one missing shutter interruption) every whole second. Combining this time mark with radiometric light curve provides absolute timing for each shutter break. The time scales from other cameras are then adjusted using the bolide lengths. This way all cameras are combined to obtain length as a function of absolute time, from which the bolide velocity and, possibly, deceleration can be computed.

The velocity near bolide beginning could be measured only on Stará Lesná digital photograph (starting from height 82 km) and Sibiu video (from 75 km). Due to its lower sensitivity, Stará Lesná film photograph starts at 64 km. On the other hand, the film camera is the only one which provides velocity data during the bright phase of the bolide, down to 40 km. The Gornovita and Vošlobeni videos provided really useful velocity data only at heights 59–53 km and Cluj-Napoca at 56–48 km. We obtained bolide velocity $27.76 \pm 0.19 \text{ km s}^{-1}$ from linear fit to the time-length data combined from all cameras. Figure 10 shows the deviations of individual length measurements from the length expected for this velocity and the given time.

Using the Vošlobeni data only, velocity as high as 30 km s$^{-1}$ could be obtained. However, this is a result of relatively poor calibration of this video and difficulties of measurement of the bolide in the bright phase. Cameras which recorded larger part of the bolide, namely both cameras from Stará Lesná and the Sibiu video, clearly show that the velocity was lower. Other videos also agree with this lower velocity. There is no sign of deceleration (within the precision of measurements) down the height of 40 km.

Using the radiant given in Table 3 and the atmospheric entry velocity of $27.76 \text{ km s}^{-1}$, the pre-impact heliocentric orbit was computed by the method of [Ceplecha (1987)]. The resulting orbital elements are given in Table 4. The geocentric velocity was $25.6 \pm 0.2 \text{ km s}^{-1}$. The orbit has high eccentricity and relatively low inclination. According to the Tisserand parameter, it can be classified as an asteroidal orbit, although it is close to the boundary with Jupiter family comets at $T_{\text{Jup}} = 3.05$ (Tancredi 2014). The orbit is also close to the 7:2 resonance with Jupiter located at 2.25 AU.

5. Meteorite searches

It was obvious from the beginning that the Romanian bolide does not represent a typical meteorite-dropping event. The entry speed was relatively high and the bolide end was quite sudden and occurred at high altitude. Nevertheless, meteorites were recovered before from superbolides of entry speeds of ~ 28 km s$^{-1}$ and end heights above 50 km [Borovička et al. 2015]. It was
therefore not entirely hopeless to search for them also in this case. In case of success, the meteorite-dropping-bolide end heights would be just extended to somewhat higher altitudes. More importantly, it would be interesting to learn what kind of material caused this unusual superbolide.

From the character of the bolide we could not expect any large meteorites. The asteroid was obviously completely disrupted near the bolide end. Nevertheless, the initial mass was quite large, so there was a possibility of large number of small meteorites (we expected sizes up to few centimeters at maximum, mostly smaller). The possible impact area was computed using the dark flight code of Ceplecha (1987) and high atmosphere winds measured by the Bucharest radiosonde at 0 UT. Although the bolide ended over mountains, the wind moved possible meteorites to the flat region in the east. The most probable impact area was found to be a 2.5 km long and 0.5 km wide strip between 45.707° N, 27.114° E and 45.730° N, 27.120° E. Meteorite masses should increase in the northern direction. Most of the area is cultivated fields but a part of village Pietroasa, belonging to nearby Câmpineanca, lies also within it.

It was a freezing weather and snow was lying on the ground during the event on January 7. Shortly after that, the snow melted and there were periods of rain and snowfall before the weather improved in the spring. Two expeditions of five and seven people, respectively, were organized into the suspected impact area on March 26, and on April 3, 2015. Searches were performed visually and with metal detector. The conditions were favorable with flat terrain and little vegetation. Of course, only small part of the suspected area could be searched. The results were negative. The mayor of Câmpineanca and several local people were interviewed. Nobody was aware of any recovered fragments.

6. Bolide light curve

Figure 11 shows the brightness of the bolide in absolute magnitudes as a function of time. The raw radiometric records shown in Fig. 11 were converted into stellar magnitudes taking into account the response as a function of zenith distance (measured in laboratory), the range to the bolide, and atmospheric extinction. Since radiometers provide signal as a function of time, bolide position as a function of time must be computed to obtain bolide range and zenith distance. For that purpose the bolide trajectory and constant velocity as determined in previous sections were used. Note that this approach may lead to somewhat underestimated brightness of the bolide trail at the end of the light curve since the trail did not continue the forward motion. Radiometric curve is provided in the supplementary file lightcurve.txt.

The radiometers have different sensitivities and are not calibrated in absolute sense. To obtain absolute magnitudes, radiometric curves were shifted to overlap with the light curves obtained from Stará Lesná photographs. Photographic light curves were calibrated using stars. Their scatter is, however, larger and temporal resolution is lower than for radiometers. Moreover, the photographs became saturated when bolide brightness increased too much. Although saturation correction was applied, the precision in the saturated part is poor. The digital photograph became saturated when the bolide absolute magnitude reached −16 and no measurements were possible at all above magnitude −18. The film camera was saturated above magnitude −19.

It can be seen in Fig. 11 that the agreement between independent measurements on digital and film cameras is reasonably good. The digital camera is generally more precise. To adjust the radiometric scale, the part of the digital light curve where the bolide brightness was

Table 4: Heliocentric orbit (J2000.0)

| Parameter                        | Value               |
|----------------------------------|---------------------|
| Semimajor axis                   | 2.27 ± 0.06 AU      |
| Eccentricity                     | 0.785 ± 0.006       |
| Perihelion distance              | 0.489 ± 0.004 AU    |
| Aphelion distance                | 4.06 ± 0.12 AU      |
| Inclination                      | 12.17° ± 0.11°      |
| Argument of perihelion           | 98.2° ± 0.5°        |
| Longitude of the ascending node  | 106.199°            |
| Tisserand parameter to Jupiter    | 3.09 ± 0.06         |

Figure 11: Light curve of the January 7 bolide determined from four radiometers, one digital photograph and one film photograph. The numbers give bolide height in km at the corresponding time.
about $-15$ mag was used. Here the signal was high but not saturated yet, so the uncertainty is the smallest.

The extinction correction was very important because the bolide was quite close to the horizon. Note that extinction correction must be performed differently for cameras and radiometers. For cameras, we used the formula of Rozenberg (1966) to compute the airmass, $X$, as a function of zenith distance, $z$:

$$X = \left( \cos z + 0.025 \exp(-11 \cos z) \right)^{-1}. \quad (1)$$

Radiometers, however, do not observe just the bolide. They capture all light coming to the station, including bolide light scattered by the atmosphere. The signal therefore does not decrease so much when the object is close to horizon. This fact was discussed by Krisciunas and Schaefer (1991). Using the rising full Moon, we found the following simple formula appropriate for radiometric measurements at low elevations:

$$X_{\text{scatt}} = \left( \cos z + 0.1 \right)^{-1}. \quad (2)$$

The extinction correction is $\Delta m = kX$, where the extinction coefficient $k$ was assumed to be the same for cameras and radiometers. It was determined using stars on the digital camera ($k = 0.25$ mag).

Although the three detectors (panchromatic film, digital camera, and photomultiplier used in the radiometers) have slightly different spectral responses, the maximum always lies in visual range. The measured magnitudes can be therefore regarded as visual magnitudes.

As it can be seen in Fig. 11, the bolide light curve was smooth at the beginning. The initially quick increase of brightness was followed by a slower brightening. A short asymmetric flare with steep onset occurred at the height of 53 km. A much more significant onset of brightness started at the height of 48 km. The rest of the bolide was a gigantic flare with several submaxima. The peak brightness of absolute magnitude $-21.0 \pm 0.3$ occurred at the height of 42.7 km, in good agreement with the position of the brightest spot in the trail. The brightness started to drop quickly at time 1:07:58.85, which corresponds to height 41.5 km, assuming no bolide degradation. Most of the radiometric signal after 1:07:59 UT was due to the stationary bolide trail. The trail luminosity was supposedly produced by a column of hot vapor, which was initially optically thick. Its luminosity could be also supported by continuing ablation of fine dust.

7. Fragmentation model

The bolide light curve was modeled using the fragmentation model developed for the Košice meteorite fall (Borovička et al., 2013). Every flare can be explained by a fragmentation event accompanied with a release and evaporation of a number of small fragments. The complex light curve could be therefore modeled relatively easily assuming that every increase of brightness was caused by a loss of certain amount of mass in form of small fragments. The fragment mass range can be estimated from the slope of the brightness onset and from the duration of the flare. Within that range, the power law distribution with mass distribution index $s = 2$ was assumed. In addition to instantaneous release of fragments, gradual release was also allowed. In that case the rate of fragment release was described by the erosion coefficient, an analogy of the ablation coefficient describing the evaporation rate (see Borovička et al., 2013).

The modeled light curve is shown in Fig. 12. Luminous efficiency was assumed to depend on fragment velocity and mass. We used the velocity- and mass- functions of ReVelle and Ceplecha (2001), normalized so that the luminous efficiency at 15 km s$^{-1}$ was 5% for large fragments ($\gg 1$ kg) and 2.2% for small fragments ($\ll 1$ kg). The conversion factor 1500 W for zero magnitude meteor (Ceplecha et al., 1998) was used to convert magnitudes into the radiated energy (bolometric). The initial mass of the asteroid was estimated to be 4500 kg. Considering the uncertainty in photometry and lu-
Table 5: Entry parameters of four superbolides compared in this study.

| Name    | Mass$^a$ | Speed | Slope | Material  | Density $^b$ |
|---------|----------|-------|-------|-----------|-------------|
| Koˇsice | 3500 kg  | 15.0  | 60°   | H5        | 3400 kg/m³  |
| Maribo  | 2300 kg  | 28.3  | 31°   | CM        | 2100 kg/m³  |
| Taurid  | 1300 kg  | 33.1  | 17°   | Comet     | 800 kg/m³   |
| Romanian| 4500 kg  | 27.8  | 43°   | ?         | ?           |

$^a$Photometric mass estimate; $^b$Kohout et al. (2014); $^c$Britt and Consolmagno (2003); $^d$Sosa and Fernández (2009)

In order to evaluate how typical or exceptional the behavior of the Romanian superbolide was, we will compare it with three other superbolides with comparable brightness, for which we have radiometric light curves and fragmentation model could be constructed. The list of all compared bolides and their entry parameters are given in Table 5. Figure 13 shows calibrated radiometric light curves of all four bolides and Fig. 14 shows their heliocentric orbits. We first describe the events individually and then compare them.

8.1. Koˇsice

The Koˇsice meteorite fall occurred in Slovakia on February 28, 2010. The meteorites are ordinary chondrites of type H5, i.e. a very common type of stony meteorites. The bolide was studied in detail by Boroviˇcka et al. (2013). The trajectory and orbit was determined on the basis of three casual video records. Radiometric curve from distant EN stations was also available and was used for modeling atmospheric fragmentation. We take here the results of Boroviˇcka et al. (2013). The maximum magnitude $-18$ was reached relatively high (at 36 km) but the end height of only 17.4 km corresponds to strong meteoritic material.
8.2. Maribo

The Maribo meteorite fall occurred in Denmark on January 17, 2009. The meteorite is a carbonaceous chondrite of type CM, i.e., one of the softest known types of meteorites with density significantly lower than for ordinary chondrites (Britt and Consolmagno, 2003). The meteorite and the circumstances of its fall were described by Haack et al. (2012). The bolide trajectory, velocity, and orbit were estimated by several authors (see Schult et al., 2015). The results of an independent analysis of one casual video from Sweden, one distant all-sky image from the Netherlands, radar data from Germany and radiometric light curves from seven Czech stations have been included in Borovička et al. (2015). All authors agree that the initial velocity was close to 28 km s\(^{-1}\). It was surprising that meteorite of such a fragile type survived the atmospheric entry with such a high entry velocity. The maximum magnitude was \( -19 \) so the bolide falls into superbolide category. The maximum height (81 km) and end height (58 km) are very large and the event is a good example of the entry of an extremely fragile cometary body, which was completely destroyed at high altitudes and no meteorite reached the ground. The bolide belonged to the Taurid meteor shower. The parent body of this shower is comet 2P/Encke with the most probable density of 800 kg m\(^{-3}\) (Sosa and Fernández, 2009).

8.3. Taurid bolide of October 31, 2015

We selected for the comparison also a very bright Taurid bolide, which occurred over northern Poland on October, 31, 2015, at 18:05:20 UT. The bolide was studied by Olech et al. (2016) and independent analysis using EN data including radiometric curves was performed by Spurný et al. (in preparation). We present here the light curve and fragmentation model. The initial mass was slightly lower than in other cases but still well above 1000 kg. The maximum magnitude was \( -18.6 \), so the bolide falls into superbolide category. The maximum height (81 km) and end height (58 km) are very large and the event is a good example of the entry of an extremely fragile cometary body, which was completely destroyed at high altitudes and no meteorite reached the ground. The bolide belonged to the Taurid meteor shower. The parent body of this shower is comet 2P/Encke with the most probable density of 800 kg m\(^{-3}\) (Sosa and Fernández, 2009).

8.4. The comparison

First we note that the orbits of all four bolides (Fig. 14) can be characterized by low inclinations and aphelia between 4–4.5 AU. Based on the orbits only, significant differences in material type and, consequently, atmospheric behavior, could not be expected. Perhaps, the only indication of different origin could be the somewhat lower eccentricity of the Košice H5 chondrite.

The light curves in Fig. 13 have different character but light curves are influenced by entry speeds and trajectory slopes, which varied from case to case (Table 5). To reveal different material properties we have to compare fragmentation behavior in the atmosphere. A good illustration of the fragmentation process is plotting the mass of the largest remaining fragment as a function of increasing dynamic pressure during the atmospheric entry.
dynamic pressure acting on the body. Dynamic pressure, given by \( p = \rho v^2 \), where \( \rho \) is density of the atmosphere and \( v \) is velocity, describes the actual mechanical action of the atmosphere on the body. Using dynamic pressure as the independent variable enables us to compare bolides with different slopes and speeds. In fact, the actual dynamic pressure is \( \Gamma \rho v^2 \), where \( \Gamma \) is the drag coefficient. Since the value of \( \Gamma \) is not known, but is probably similar in all cases (about 0.5), we use \( \rho v^2 \) for simplicity.

We can see in Fig. 15 that the Taurid body started to lose the mass intensively under very low dynamic pressures \(<0.01 \text{ MPa} \) and was completely destroyed at 0.1 MPa. It was evidently much more fragile than the other three bodies, though its strength was still much larger than 25 Pa expected for a rubble pile (Sánchez and Scheeres 2014). The Romanian body lost only negligible amount of mass before the dynamic pressure reached 0.9 MPa. In that respect it was even more resistant than Koševo, which lost almost half of mass at 0.1 MPa. Maribo was loosing mass in repeating fragmentation events. At the time when dynamic pressure reached 0.9 MPa, about 75% of Maribo mass was lost.

After the dynamic pressure exceeded 1 MPa, the Romanian body started to disrupt severely. No fragment larger than 10 grams probably survived pressures above 3 MPa. Although Koševo also disrupted at 1 MPa, the difference is, that many macroscopic fragments survived the disruption and some large fragments (\( \geq 10 \text{ kg} \)) survived the maximal pressure of almost 6 MPa. They were then decelerated and dynamic pressure therefore started to decrease, while ablation, and possibly also some fragmentation, continued. The largest recovered meteorite had a mass of 2.37 kg (Borovička et al. 2013; Šteha et al. 2015). Maribo fragmented most severely at 3–4 MPa (the exact value is uncertain because of lack of detailed deceleration data). The mass of the only recovered meteorite was 26 g and we do not think that any meteorites of significantly larger mass landed.

We also included in Fig. 15 two older superbolides observed by EN cameras, namely the ~21.5 magnitude Šumava (December 4, 1974) and the ~19.5 magnitude Benešov (May 7, 1991) (Borovička and Spurný 1996). Since radiometric light curves are not available in these cases, detailed fragmentation models could not be constructed. For Šumava we plotted the original analysis of Borovička and Spurný (1996). For Benešov, the recent re-evaluation of the early-stage fragmentation (Borovička 2016b) was used.

Šumava, also a member of the Taurid complex, was a fragile body. As it can be seen in Fig. 15, it resisted fragmentation little bit more than the EN 311015 Taurid, nevertheless, was completely destroyed at dynamic pressure of the order of 0.1 MPa. Benešov was a deeply penetrating bolide and dropped stony meteorites, which, surprisingly, were of different mineralogical types (Spurný et al. 2014). The body disrupted into small pieces (~ 40 kg) at even lower pressure than Šumava but the small pieces survived until pressures 2–9 MPa. Both meteorite recoveries and atmospheric behavior suggest that Benešov was a weakly bound conglomerate of intrinsically relatively strong components. It was probably a product of a collision of asteroids of different compositions.

Koševo was an example of a cracked body made from an intrinsically strong material. The Romanian body behaved differently. There were apparently no large scale failures (cracks). Most of the body remained intact until 1 MPa. After that, however, the body disrupted into quite small fragments or dust. It seems that the intrinsic material strength was of the order of 1 MPa. This is almost two orders of magnitude lower strength than for pristine (uncracked) ordinary chondrites (Popova et al. 2011) and almost two orders of magnitude higher strength than for material from comet Encke. One may speculate that the Romanian body was an carbonaceous asteroid. Maribo, however, showed different behavior with many separate fragmentation events over a wide range of dynamic pressures from ~ 5 kPa (where only 1% of mass was lost; more severe fragmentations started at 20–30 kPa) to a few MPa. That behavior suggests a hierarchical structure. It seems more likely that the Romanian bolide represents a different type of asteroidal material, which is not represented in meteorite collections. It is weak but structurally homogeneous.

9. Discussion

9.1. US Government sensor data

We were able to provide reliable trajectory and velocity data for the January 7, 2015, superbolide observed over Romania. This superbolide was detected also by the US Government sensors (USGovS). The data were used by Brown et al. (2016) in their study of meter-scale impactors. Unfortunately, the speed reported by the USGovS (35.7 km s\(^{-1}\)) was by 8 km s\(^{-1}\) (almost 30%) larger than the real speed. The derived orbit was distinctly cometary with Tisserand parameter \( T_J = 1.75 \) and aphelion at 9.2 AU. In reality, the aphelion was just above 4 AU and the orbit can be classified as asteroidal. This example shows that big care must be taken when using the USGovS data.
We can compare also other quantities reported for this event at the USGovS bolide webpage[1] and in Brown et al.[2016]. The radiant position (R.A. = 119.8°, Decl. = +7.0°) is off by seven degrees, which is also significant for orbit computation. Bolide location is given only to one decimal point (45.7N, 26.9E) and is correct within that precision. The reported height of maximum (45.5 km) is too high by 2.7 km. It lies, nevertheless, within the bright phase of the bolide (see Fig. 12). The total impact energy was reported to be 0.4 kt TNT. Our mass (4500 kg) and speed (27.76 km s$^{-1}$) is too high by 2.7 km. It lies, nevertheless, within the bright phase of the bolide (see Fig. 12). The total impact energy was reported to be 0.4 kt TNT. Our mass (4500 kg) and speed (27.76 km s$^{-1}$) give 1.7 × 10$^{12}$ J = 0.41 kt TNT. Since our mass estimate is rather uncertain, this is a surprisingly good agreement.

The bolide position and energy reported by the USGovS seems therefore to be more reliable than the velocity vector. Note that Košice bolide was observed by the USGovS as well. The speed agrees within 0.1 km s$^{-1}$ in this case and the radiant difference is only 4 degrees.

9.2. Derivation of asteroid structure from superbolide data

The main topic of this paper was the study of the structure and strength of small asteroids using superbolide data. We modeled high resolution radiometric light curves with the knowledge of bolide trajectories and speeds. The aim was to reveal atmospheric fragmentation history. We have to note that the models are not unambiguous and the light curves could be probably reproduced with different sets of parameters. Nevertheless, the main characteristics, especially the heights of mass loss events and the amount of mass lost in form of small quickly evaporating fragments, can be revealed well. These characteristics are sufficient to study structural differences among impacting asteroids. We cannot be sure about the number and masses of macroscopic fragments. For that purpose detailed video records showing the motion of individual fragments would be desirable. Such data are very rare. One example was the Morávka meteorite fall [Borovicka and Kalenda, 2003], where, however, sufficiently good light curve was missing. It could be partly supplemented by good seismic data, which also contain information about fragmentation events.

Unfortunately, data available for most superbolides are very limited. Brown et al.[2016] used the height of maximum as a proxy of asteroid strength. Our small sample shows that bodies with quite different material properties can have similar peak height. Peak height is therefore poor discriminator of material strength. Extremely fragile (cometary) or very strong bodies can be distinguished but nothing can be said about the majority of events with intermediate peak heights.

The end height is a better discriminator (Košice 17 km, Maribo 31 km, Romanian event 39 km if neglecting the most detailed video, Taurid 58 km). However, end height is more dependent on observational techniques and circumstances and is not available at all in the USGovS data. The classical PE criterion [Cephecha and McCrosky, 1976] is based on end height, although the entry mass, speed, and angle must be also taken into account. This criterion was, nevertheless, developed for ordinary bolides and may lead to misleading results when applied to superbolides. The Romanian event would be classified as type IIIB, i.e. soft cometary material, using the PE criterion, even if the end height of 36 km from the most detailed video were used. The Taurid would be also IIIB, while Maribo and Košice fall into type II. Note that the original luminous efficiency of Cephecha and McCrosky [1976] must be used when computing the entry mass for the PE formula (it can be found also in Cephecha [1988]). The modern luminous efficiency for bolides is higher [ReVelle and Cephecha, 2001]. Cephecha [1994] used the old luminous efficiency and overestimated the masses and sizes of the studied meteoroids.

Bolide end heights were recently discussed also by Moreno-Ibáñez et al.[2015]. Their methodology, however, relies on observed deceleration along the trajectory and does not take into account bolide luminosity, and is therefore not suitable in the present cases.

10. Conclusion

The main conclusion of this paper is the large structural diversity of meter-sized asteroids. Although many types of meteorites are known, from the point of view of structure and density, there are just three main types: metals, silicate-rich stones, and carbonaceous stones. Of course, asteroids of cometary origin with low density and strength are also expected to exist. The Romanian event, however, probably did not belong to any of these types. The bulk strength and the material strength were both of the order of 1 MPa. We expect the material to have high microporosity but not so high as cometary materials. Judging from the orbit, the Romanian asteroid probably originated in the middle or outer asteroid belt.

The implication of large structural diversity of small asteroids is difficulty of predicting impact consequences
for an asteroid of known size but unknown material properties.

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Appendix A. Supplementary files

The video records of the January 7 bolide used in our analysis are provided as supplementary files to the online version of this article. The list of the files is given in Table 6. Note that the files are meant mostly for illustrative purposes. Although care was taken to preserve video quality, slight deterioration or deformation may have occurred when converting between different formats and codecs. In case of Eforie Sud we were able to provide for technical reasons the video in two limited versions only; one with lower resolution and one with limited number of frames.

In addition, we provide the derived coordinates (azimuths, zenith distances) of the bolide as seen from the individual sites, and the radiometric light curve. Both are given as self-explanatory text files, coordinates.txt and lightcurve.txt, respectively.

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Table 6: List of supplementary video files

| File               | Video site         | Credit                  | Note                |
|--------------------|--------------------|-------------------------|---------------------|
| Cluj-Napoca.mp4    | Cluj-Napoca, Câmpul Păini str. | SECPRAL COM           |                     |
| EforieSud-small.avi | Eforie Sud         | High School “Carmen Sylva” | low resolution |
| EforieSud-3fps.avi  | "                  | "                       | low frame rate      |
| Fierbinti.mp4      | Fierbinti, Nordului str. | Adrian Pascale          | color               |
| Gornovita.avi      | Gornovita observatory | Marian Lucian Achim    |                     |
| Sibiu.avi          | Sibiu Municipal Stadium | Sibiu City Hall        |                     |
| Voslobeni.avi      | Voslobeni, Heveder str. | Balint Ede             |                     |

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