The impact of AGN feedback and baryonic cooling on galaxy clusters as gravitational lenses

James M. G. Mead\textsuperscript{1,2}**, Lindsay J. King\textsuperscript{1,2}†, Debora Sijacki\textsuperscript{1,2}, Adrienne Leonard\textsuperscript{1,2,3} Ewald Puchwein\textsuperscript{4} and Ian G. McCarthy\textsuperscript{2,1,5}

\textsuperscript{1}Institute of Astronomy, University of Cambridge, Madingley Rd, Cambridge CB3 0HA
\textsuperscript{2}Kavli Institute for Cosmology, University of Cambridge, Madingley Road, Cambridge CB3 0HA
\textsuperscript{3}Service d’Astrophysique, CEA Saclay, 91191 Gif-sur-Yvette Cedex, France
\textsuperscript{4}Max-Planck-Institut für Astrophysik, Karl-Schwarzschild-Straße 1, 85741 Garching, Germany
\textsuperscript{5}Astrophysics Group, Cavendish Laboratory, Madingley Road, Cambridge CB3 0HE

ABSTRACT

We investigate the impact of AGN feedback on the gravitational lensing properties of a sample of galaxy clusters with masses in the range \(10^{14} - 10^{15}\) \(M_\odot\), using state-of-the-art simulations. Adopting a ray-tracing algorithm, we compute the cross-section of giant arcs from clusters simulated with dark-matter only physics (DM), dark matter plus gas with cooling and star formation (CSF), and dark matter plus gas with cooling, star formation and AGN feedback (CSFBH). Once AGN feedback is included, baryonic physics boosts the strong lensing cross-section by much less than previously estimated using clusters simulated with only cooling and star formation. For a cluster with a virial mass of \(7.4 \times 10^{14} M_\odot\), inclusion of baryonic physics without feedback can boost the cross-section by as much as a factor of 3, in agreement with previous studies, whereas once AGN feedback is included this maximal figure falls to a factor of 2 at most. Typically, clusters simulated with DM and CSFBH physics have similar cross-sections for the production of giant arcs. We also investigate how baryonic physics affects the weak lensing properties of the simulated clusters by fitting NFW profiles to synthetic weak lensing data sets using a Markov Chain Monte Carlo approach, and by performing non-parametric mass reconstructions. Without the inclusion of AGN feedback, measured concentration parameters can be much larger than those obtained with AGN feedback, which are similar to the dark-matter only case.

Key words: cosmology: observations - cosmology: theory - galaxies: clusters: general - gravitational lensing: numerical

1 INTRODUCTION

In recent years, strong gravitational lensing by galaxy clusters has been used to investigate cosmological problems and to improve our understanding of cluster physics. Strong lensing can manifest itself as highly non-linear distortions of light from background galaxies (giant arcs) and observational searches have revealed many spectacular examples around both optically-selected and X-ray-selected clusters (e.g. Zaritsky & Gonzalez (2003), Gladders et al. (2003)). It has been found that the strong lensing properties of clusters depend on myriad physics - including the cosmological parameters, halo substructure and baryonic physics. Strong lensing is hence a good technique to investigate both cosmology and cluster physics.

The frequency of giant arcs around galaxy clusters is sensitive to the cosmological model. Using dark matter simulations, Bartelmann et al. (1998) (henceforth B98) found that in \(\Lambda CDM\) the number of giant arcs is a factor of 5-10 lower than in observations. This disparity arises either because our cosmological model is incorrect or, more likely, that some aspects of the modeling of the source or lens populations are incorrect, for example that we are missing crucial physics from our cluster simulations.

A substantial body of work has investigated this latter point, using increasingly sophisticated simulations in order to reconcile predictions with observations. There have been a number of papers investigating the strong-lensing properties of dark matter-only clusters (e.g. Ho & White (2005).
The earliest analytic work focused on spherically symmetric cluster models, but it has been demonstrated that halo triaxiality has a strong impact on arc production e.g. by Oguri et al. (2003), who used semi-analytic models, and in a complementary analysis by Dalal et al. (2004) who analysed a simulated cluster sample.

Other papers have also considered the impact of baryonic physics, in particular models including gas with cooling and star formation, and cluster galaxies. Baryons can have a significant impact on the central regions of galaxy clusters, and since it is precisely this region that is important in arc production, one would expect the abundance of giant arcs to be sensitive to the baryonic physics of the cluster. Puchwein et al. (2005), Wambsganss et al. (2007) and Rozo et al. (2008) found that the addition of baryons to cluster simulations increases the lensing cross-section by factors of a few. Of the cluster galaxies, only the central cD galaxy makes a non-negligible contribution to the strong lensing properties, increasing cross-section by up to 50% (Meneghetti et al. 2003).

The baryonic cluster simulations which have been used to date in the prediction of lensing cross-sections suffer from significant over-cooling, with much higher stellar fractions than observed (see the discussion in e.g. Puchwein, Sijacki & Springel 2008, Balogh et al. (2001) and Puchwein et al. (2010)). In the absence of heating, the central regions of clusters cool faster than the outer regions, causing gas to flow inward in a quasi-hydrostatic cooling flow; this would result in a large quantity of cold gas in the central regions of clusters, a high star formation rate, and extremely luminous central galaxies. However, this is at odds with both observations of clusters, which do not show such strong cooling flows, and also of Brightest Cluster Galaxies (BCGs) that tend to have evolved, red, stellar populations. There is compelling evidence from observational and theoretical work that the AGN feedback processes that accompany the accretion of gas onto supermassive black holes - residing in most galaxies - provide a heating mechanism that prevents over-cooling, bringing physical models of clusters more into line with observations (e.g. Valageas & Silk 1999, Bower et al. (2001), McNamara & Nulsen (2007), McCarthy et al. (2009); Croton et al. (2006)).

It is well established that strong lensing cross-sections can be used to probe the central density profiles of clusters - steeper slopes of inner density profiles enhance arc production capability, e.g. Meneghetti et al. (2007). Torri et al. (2004) investigated the effects of cluster mergers on the strong lensing cross-section, finding that during a merger the cross-section can be amplified by up to an order of magnitude. The cross-section for strong lensing can also be boosted by as much as 50% for lower mass clusters by line-of-sight structure (Puchwein & Hilbert 2009). An additional factor that can affect the cross-section are the properties of the background galaxies themselves, such as their redshift distribution, size, shape and clustering, e.g. Wambsganss et al. (2004); Li et al. (2005); Gao et al. (2009).

Departures from ΛCDM have also been invoked to reconcile the observed abundance of arcs with the value of σ₈ (~ 0.8) consistent with cosmic shear surveys and CMB observations from WMAP. For example, Bartelmann, Doran & Wetterich (2006) consider early dark energy (EDE) cosmologies, where there is significant dark energy even at very early epochs, unlike the case of ΛCDM or many simple quintessence models. Their analytic predictions suggest that non-linear structure formation can be substantially enhanced beyond that of ΛCDM. Fedeli et al. (2008) suggest that EDE has a significant impact on the statistics of giant arcs, bringing predictions and observations into closer agreement. More recently, Francis, Lewis & Linder (2009) and Grossi & Springel (2009) carried out the first studies of non-linear structure formation in EDE models using N-body simulations, finding its impact to be much more difficult to detect observationally than implied by analytic models.

There has also been interest in the effects of baryonic physics on the weak lensing properties of clusters. Future large surveys, such as the Dark Energy Survey (DES: https://www.darkenergysurvey.org/) will measure the matter power spectrum with unprecedented precision, also allowing stringent constraints to be placed on the properties of dark energy (Albrecht et al. 2006). Studies by, for example, Rudd et al. (2007) and White (2004), have indicated that the inclusion of baryonic physics can have a significant effect on the weak lensing properties of clusters, and hence would significantly alter the predictions for the matter power spectrum relative to those simulations which include only dark matter.

It is essential to understand the impact that baryonic physics and AGN feedback might have on the gravitational lensing properties of galaxy clusters in order to calibrate constraints on their physical properties, and fully exploit their potential as cosmological probes. This is important both for the interpretation of existing data, and to prepare for upcoming large surveys such as DES. In this paper we seek to extend the picture of cluster lensing by investigating the influence of AGN feedback on the lensing properties of numerically simulated clusters. We use recent state-of-the-art simulations from Puchwein, Sijacki & Springel (2008) that incorporate the growth of black holes (BHs) and corresponding feedback processes using the prescription detailed in Sijacki et al. (2007). These are the first cosmological simulations of clusters to incorporate AGN feedback self-consistently. We use these simulations to demonstrate the impact that realistic modelling of AGN physics can have on cluster lensing results.

Throughout this paper a ΛCDM cosmology with parameters Ω_m = 0.25, Ω_Λ = 0.75 and H_0 = 73km s⁻¹Mpc⁻¹ is adopted. The paper is organized as follows. In Section 2 the cluster simulations that are used are described. The numerical methods for the creation of synthetic arcs using strong lensing ray-tracing through the simulated clusters, and the generation of weak lensing catalogues are outlined in Section 3. The impact of baryonic physics on the strong-lensing and weak-lensing properties of the clusters are presented in Section 4 and in Section 5 respectively. Finally, in Section 6 the significance of our findings in the context of previous work is discussed.
star formation (CSF) and the latter with added AGN feedback (CSFBH). The mass range was chosen to be large enough to investigate any strong mass dependence of lensing properties on baryonic physics. The virial masses and radii of these clusters are summarised in Table 1. The virial mass and radius are taken to be equivalent to $M_{200}$ and $r_{200}$, defined by the mass enclosed inside the radius within which the mass density is 200 times that of the critical density of the universe at the redshift of the cluster. Note that in Table 1, clusters are designated C1-C5 in order of increasing $M_{200}$ with respect to the background density. The cluster sample is taken from Puchwein, Sijacki & Springel (2008), in which the simulations are based on the numerical prescription described in Sijacki et al. (2007). Puchwein, Sijacki & Springel (2008) selected clusters from the dark-matter-only Millennium simulation (Springel et al. 2005a), and performed a number of re-simulations that incorporated baryonic physics with and without AGN feedback. DM clusters that are used in this paper were not already available at high a resolution as the CSF and CSFBH runs, so these were re-simulated using the same process as in Puchwein, Sijacki & Springel (2008) (summarised in Section 2.1). In Section 2.2 we recap on the numerical code, and in Section 2.3 the black hole model is discussed in more depth.

### 2.1 Re-simulating Millennium Clusters

The re-simulations were performed by selecting the Lagrangian region of the target halo and then populating it with a larger number of lower mass particles, adding small-scale power up to the new Nyquist frequency. At larger distances outside this high-resolution region, increasingly more massive particles were used, ensuring that the gravitational tidal field acting on the high resolution region is accurately represented. For the simulations with gas, each high-resolution dark matter particle is split into a dark matter particle and a gas particle, displacing them by half of the original mean inter-particle separation. The centre of mass of each pair is fixed.

### 2.2 The Numerical Code

The simulation of the cluster sample in Puchwein, Sijacki & Springel (2008) follows the same prescription as in Sijacki et al. (2007) and readers are referred to this paper for more details on the simulation and black hole (BH) model. The Tree-SPH code GADGET-3 is used (based on Springel (2005)), which includes gravity and non-radiative hydrodynamics of dark matter and gas components, and also follows radiative cooling and heating of an optically thin plasma of hydrogen and helium. A sub-resolution multiphase model for star formation and the associated supernova feedback was adopted (Springel & Hernquist 2003). The growth and feedback processes of a population of BHs embedded in the simulations were self-consistently followed, and this process is described in section 2.3.

### 2.3 The Black Hole Model

In the simulations, BHs are represented as collisionless sink particles which can accrete gas from their surroundings. Any halo above a threshold mass of $5 \times 10^{10} h^{-1} M_\odot$ is seeded with a BH of mass $10^7 h^{-1} M_\odot$, if it does not contain a BH already. The growth of this BH population through accretion is then followed. The accretion rate of the BH follows the spherically symmetric Bondi-Hoyle-Lyttleton model (Hoyle & Lyttleton 1939, Bondi & Hoyle 1944, Bondi 1952): 

$$M_{\text{BH}} = \frac{4\pi \alpha G^2 M_{\text{BH}}^2 \rho}{(c_s^2 + v^2)^{3/2}},$$

where $\alpha$ is a dimensionless parameter ($\alpha = 100$ in the simulations we use), $\rho$ is the density, $c_s$ is the sound speed of the gas and $v$ is the velocity of the BH relative to the gas. In the model, the upper limit of the BH accretion rate is given by the Eddington rate.

There is one additional process through which BHs may gain mass - they are allowed to merge with other BHs that lie within the smoothing lengths used to estimate the local gas density, and have relative velocities lower than the local gas sound speed.

The model for BH feedback accounts for AGN heating at both high and low accretion rates. In the model there are two modes of AGN feedback: at high accretion rates it is assumed that the bulk of AGN heating originates in luminous quasar activity, whilst at lower accretion rates, corresponding typically to lower redshifts, AGN heating proceeds via radiatively inefficient feedback in a mostly mechanical form. The transition between these two regimes is characterized by a parameter $\chi_{\text{radio}} = M_{\text{BH}}/M_{\text{halo}}$ - for $\chi_{\text{radio}} > 10^{-2}$ we are in the “quasar” heating regime, and for $\chi_{\text{radio}} < 10^{-2}$ we are in the “radio mode” feedback regime, which is modelled by injecting bubbles into the host cluster.

In the quasar heating regime a small fraction of the bolometric luminosity is coupled thermally and isotropically to the surrounding gas particles (Springel, Di Matteo & Hernquist (2005a)), with an amount given by,

$$E_{\text{cool}} = \epsilon_l L_z = \epsilon_r \epsilon_t M_{\text{BH}} c^2.$$  

In this equation $\epsilon_t$ is the efficiency of thermal coupling and $\epsilon_r$ is the radiative efficiency. We adopt $\epsilon_t = 0.05$ and $\epsilon_r = 0.1$ as in previous work, to ensure agreement between the simulated and observed $M_{\text{BH}} - \sigma$ relation (Sijacki et al. 2007, Di Matteo et al. 2008).

In the radio mode feedback regime, below $\chi_{\text{radio}}$, accretion intermittently produces AGN jets which blow hot bubbles in the surrounding gas. The cluster simulations that we use employ a model of radio feedback in which an AGN-
driven bubble is created if a BH has increased in mass by a fraction \( \delta_{\text{BH}} \equiv \delta M_{\text{BH}}/M_{\text{BH}} \). In this case, the energy content of the bubble is,

\[
E_{\text{bub}} = \epsilon_m c^2 \delta M_{\text{BH}},
\]

where \( \epsilon_m = 0.2 \) is the mechanical feedback efficiency. The radius of the bubble is modelled by,

\[
R_{\text{bub}} = R_{\text{bub},0} \left( \frac{E_{\text{bub}}/E_{\text{bub},0}}{\rho_{\text{ICM}}/\rho_{\text{ICM},0}} \right)^{1/5},
\]

where \( R_{\text{bub},0} \), \( E_{\text{bub},0} \) and \( \rho_{\text{ICM},0} \) are normalization constants for bubble radius, energy content and ambient density.

### 3 NUMERICAL METHODS FOR LENSING SIMULATIONS

Surface mass density maps are created by projecting the matter on to a two-dimensional grid using an adaptive SPH projection algorithm. It is also possible to project using a triangular-shaped clouds (TSC) scheme. Where the particle density is high (i.e. in the strong-lensing region around the centre of the cluster) the two algorithms should produce almost identical surface densities. We verified that the choice of projection algorithm does not affect the lensing cross-sections.

The physical extents of the clusters are much less than the distances between the observer-cluster and cluster-sources, so the thin-lens approximation is valid. Each surface mass density map is determined on a 600 \( \times \) 600 grid covering a square of \( 1.5 \, h^{-1} \, \text{Mpc} \) (comoving) on a side, centred on the cluster. To create a map of the convergence (\( \kappa \)), the surface density map, \( \Sigma \), is divided by the critical surface mass density,

\[
\Sigma_c = \frac{c^2}{4\pi G} \frac{D_s}{D_{ds} D_d},
\]

where \( D_s \), \( D_d \) and \( D_{ds} \) are the observer-source, observer-lens and lens-source angular diameter distances. In Fig. [1] we show the convergence for cluster C5, with all 3 types of physics (CSF, DM, CSFBH) in 3 projections, for sources at \( z = 3 \).

#### 3.1 Ray-tracing for Strong Lensing Arc Production

The strong lensing properties of a cluster are sensitive to the mass distribution in the inner regions. We now describe how synthetic maps of distant galaxies strongly lensed by simulated clusters are obtained. The ray-tracing for the simulation of strong lensing by a cluster, that follows light rays...
between the source and observer via deflection at the cluster, is performed by an algorithm used in Leonard et al. (2009). The mapping between the source and lens (image) planes is given by the ‘lens equation’,

\[
\beta = \theta - \alpha(\theta),
\]

(6)

where \(\beta\) are the coordinates in the source plane, \(\theta\) are the coordinates in the lens plane, and \(\alpha\) are the deflection angles. The lensing deflection potential \(\psi(\theta)\) is related to \(\kappa\) through a Poisson equation,

\[
\nabla^2 \psi = 2\kappa.
\]

(7)

We can also relate \(\psi(\theta)\) to \(\alpha\) via,

\[
\nabla \psi = \alpha.
\]

(8)

Therefore it follows that \(\kappa\) can be related to \(\alpha\) in Fourier space,

\[
\tilde{\alpha}_i = -\frac{2ik_i}{k_i^2 + k^2_k} \tilde{\kappa}.
\]

(9)

To simulate strong lensing, equation [9] is used to calculate the deflection angles due to the cluster (on a grid of twice the resolution of the input convergence map). To achieve greater numerical accuracy, and to mitigate the influence of edge effects, the convergence field is zero-padded. The output of this ray-tracing program is a map containing the lensed arcs. This map is searched for arcs using the algorithm presented in Horesh et al. (2005). The algorithm makes calls to SExtractor (Bertin & Arnouts 1996), using slightly different detection parameters in each call, to detect objects with an axis ratio above a given value. The arc length-to-width ratio is measured as in Miralda-Escudé (1993).

The giant arc cross-sections are computed using a Monte Carlo approach. The cluster field is populated with background galaxies placed at randomly assigned positions, with exponential profiles and elliptical shaped isophotes drawn as Gaussian random deviates, as described in Leonard et al. (2009). This galaxy population is placed at uniform redshift, \(z_k = 3\) - although the redshift distribution of the source galaxy population is important for determining the absolute cross-section, in this work we are interested in the relative cross-sections of clusters simulated with different types of physics. This population of galaxies is then ray-traced through the simulation, using the methods described above. In this work, we focus on arcs with a length-to-width ratio \(r \geq 7.5\), making no distinction between tangential and radial arcs. To calculate the cross-section, 100 populations of background galaxies are simulated, each with a density of 50 arcmin\(^{-2}\), and the number of arcs produced in each realization is recorded. The cross-section is then computed by multiplying the fraction of sources that form giant arcs by the area of the cluster field over which those galaxies were distributed. An error on the cross-section is estimated by repeating this procedure 10 times (in all we simulate 1000 populations behind each cluster), and computing the standard deviations of the cross-sections.

3.2 Weak Lensing Simulations

Weak lensing is sensitive to the shear field of the cluster on larger scales. The weak lensing simulations that are undertaken to generate synthetic catalogues of weakly lensed distant galaxies behind the simulated clusters are now described. These catalogues are used to obtain NFW fits to the total mass profile, and non-parametric mass reconstructions of the target clusters.

Whereas the convergence magnifies background objects such as galaxies, the shear stretches them. The complex shear (a complex quantity with magnitude corresponding to the shear amplitude, and phase equal to twice the shear position angle) also depends on the second derivatives of the lensing potential,

\[
\gamma = \gamma_1 + i\gamma_2 = (\psi_{11} - \psi_{22})/2 + i(\psi_{12} - \psi_{21}),
\]

(10)

where commas denote partial differentiation. The complex reduced shear is obtained from the shear and convergence through the equation \(g = \gamma/(1 - \kappa)\). Using the \(\kappa\) maps corresponding to clusters simulated with DM, CSF or CSFBH physics, the corresponding maps of \(\gamma\) and \(g\) are obtained, by relating \(\kappa\) and \(\gamma\) in Fourier space given Eq. 7 and Eq. 10.

The magnification is given by the inverse Jacobian determinant of the lens equation, \(\mu(\theta) = |\det A(\theta)|^{-1}\). Evaluating this we obtain,

\[
\mu = \frac{1}{(1 - \kappa)^2 - \gamma^2}.
\]

(11)

The ellipticity of a galaxy, describing its shape and orientation, is denoted by a complex number with a modulus related to the axis ratio \(r = (1 - \tau)/(1 + \tau)\), and phase being twice the position angle. In the non-critical regime \((\delta A > 0)\) the weakly lensed image of a distant galaxy has a complex ellipticity given by,

\[
\epsilon = \epsilon^s + g^s + g^s \epsilon^s,
\]

(12)

where \(\epsilon\) and \(\epsilon^s\) are the lensed and unlensed complex ellipticities respectively, and \(g^s\) is the complex conjugate of the reduced shear (Bartelmann & Schneider 2001). Galaxy ellipticities are taken to have a Gaussian probability density function (Bartelmann & Schneider 2001),

\[
\rho_\epsilon = \frac{\exp(-|\epsilon|^2/\sigma_\epsilon^2)}{\pi\sigma_\epsilon^2 [1 - \exp(-1/\sigma_\epsilon^2)]}.
\]

(13)

Throughout this work we take \(\sigma_\epsilon = 0.2\).

In the weak-lensing analysis, the simulated background galaxies are at \(z_k = 3.0\), with random positions on the sky, and with ellipticities drawn from the Gaussian probability density function given by Eq. 13. The source galaxy redshift was chosen to be sufficiently high so as to ensure that the low mass clusters would have cross-sections significantly above zero. These galaxies are then lensed by the cluster according to Eq. 12 using the map of \(g\) corresponding to the \(\kappa\) map for a particular cluster, and taking into account any deflection due to magnification. The slope of the unlensed number counts is taken to be \(s = 0.5\), so that the local lensed number density \(n_L\) is related to the local unlensed number density \(n\) via \(n_L = n \mu^{s-1}\). We use a number density of 150 arcmin\(^{-2}\), well within the power of future surveys (Lewis & King 2006), although out of reach of present observing capabilities. With future observations we ought to be able
to probe the differences in the weak-lensing properties of clusters in great detail.

4 STRONG LENSING RESULTS

In this Section our key strong-lensing result, the effect of AGN feedback on strong lensing cross-sections, is presented. In Fig. 2 we show the spherically averaged density profiles of stars, gas and dark matter in cluster C4, simulated both with CSF and CSFBH. The stellar density is much higher in the CSF run in the central regions of the cluster - a result of the ‘overcooling problem’. Also note that the dark matter density profile has contracted in the CSF simulation relative to CSFBH, due to the comparatively large density of baryons in the cluster centre (Blumenthal et al, (1986), Gnedin et al. (2004)).

Fig. 3 shows the image plane magnification for sources at $z_g = 3$ in the inner $0.75 h^{-1}$ Mpc of the most massive cluster C5 with CSF, CSFBH and DM physics, calculated using Eqn. 11 from the convergence and shear maps. The observed properties of strongly lensed arcs depend on the distribution of magnification.

4.1 The impact of baryonic physics on cross-section

The ratios of the cross-sections were calculated for DM, CSF and CSFBH clusters and the results are summarised in Fig 4. Using a source plane definition for arc cross-section, Rozo et al. (2008) and Puchwein et al. (2005) found that the inclusion of baryonic cooling boosted cross-sections of the most massive clusters by factors of approximately 2-4 above those of DM clusters. We can see that the results of this paper are broadly in agreement with this result - for instance the CSF cross-sections of C5 exceed those of the DM simulation by factors of 2-3 (Fig. 4). However, on inclusion of AGN feedback we see that for all but cluster C5, the CSFBH and DM cross-sections are comparable. Even for cluster C5, the boost in cross-section above the DM cluster gained by adding baryons tempered with AGN feedback is $< 2$. For all clusters the reduction in cross-section between CSF and CSFBH is statistically significant. For clusters C2, C4 and C5 clearly the cross section has been reduced by many times the typical error bar. The $yz$- projection of C3 is anomalous insofar as addition of AGN physics caused no notable reduction in cross-section. On closer analysis, C3 appears to be a merging cluster with large amounts of substructure close to the cluster centre - in this sense, this projection of the cluster is ‘atypical’. The results of C1 perhaps warrant closer statistical analysis; for this purpose, we can use Student’s t-test with the null hypothesis that the mean cross-section of the two samples of clusters (CSF and CSFBH) are equal. It was found that in all cases we could reject the null hypothesis with greater than 95% confidence.

The results can be explained by analyzing the density profiles of the clusters. Rozo et al. (2008), amongst others, have demonstrated that haloes with steeper inner density profiles have higher strong lensing cross-sections. Thus, the addition of baryons to clusters is expected to boost strong-lensing cross-sections, as gas condenses in the centres of these haloes, and so the density profiles are steepened significantly relative to the DM-only case (e.g. Fig. 2). In the same way, because the CSF haloes have a greater central concentration of baryons than the CSFBH haloes, the central den-
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Figure 3. Maps of the magnification for sources at $z = 3$ in the inner $0.75\, h^{-1}\, \text{Mpc}$ of the most massive cluster C5 with CSF, CSFBH and DM physics from left to right respectively. The magnification is shown on a log scale, with the values of the scale indicated on the right panel. The black contour corresponds to magnification of 2.

Figure 4. Ratios of strong lensing cross-sections for the 3 orthogonal projections of each cluster. In Fig. 4a, 4b and 4c we show the ratio of cross-sections CSFBH/CSF, DM/CSF and DM/CSFBH respectively. On the x-axis, the xy, yz and xz projections of C1 through C5 are denoted (cycling through the projections from the lowest to highest $M_{200}$ with respect to the background density).
density profile is steeper for a CSF cluster than for a CSFBH cluster. It is thus unsurprising that the CSFBH haloes prove less efficient strong lenses than CSF haloes. The redshift of background galaxies will also have an effect on the results. For background galaxies with a relatively high redshift, poor clusters with CSF gas physics could have a projected surface mass density greater than the critical density, whereas either (or both) of DM or CSFBH clusters could remain sub-critical. This would cause a bias. The results of this paper will actually be strengthened through use of a lower source redshift - CSF clusters, due to their extremely high central density, will almost always exceed critical density; it is CSFBH and DM clusters that could first drop to sub-critical levels when lower source redshifts are used - this would result in an even greater difference between CSF and CSFBH cross-sections. To check this result, the cross-sections of C4 were investigated using a background population at $z_g = 1$. In all cases the ratio between CSFBH and CSF cross-sections was reduced relative to the $z_g = 3$ case; for example, for the xy- projection, the new ratio was calculated as 0.52. As described above, the reduction will be even more pronounced for lower mass clusters.

In order to illustrate the relative effect of AGN feedback for two different clusters, in Fig. 4 the density profile of the CSF simulation divided by the corresponding CSFBH density profile is plotted for clusters C2 and C4. In C4, the density profile is affected comparatively more by the inclusion of AGN feedback, both in terms of its absolute value and its slope.

As regards to the mass trend, a much larger sample will be required to draw firm conclusions. With the exception of C5 (which is discussed below), with increasing cluster mass the ratio CSFBH/CSF decreases, whilst the ratio DM/CSFBH is approximately constant. We can physically explain these mass trends as follows. The AGN feedback is less effective in cluster C5 than C4, insofar as the CSFBH cross-section is a larger fraction of the CSF cross-section, and exceeds the DM cross-section by a greater amount. A possible explanation lies in the fact that AGN feedback does not completely overcome central gas cooling in C5. Thus, relatively speaking, the AGN feedback has less of an impact in C5 than in C4. The stellar fraction of C5, even when simulated with CSFBH, is still larger than observed in reality (Puchwein, Sijacki & Springel 2008) - if the stellar fraction were reduced in C5 to observed levels this would almost certainly result in a further reduction in the CSFBH cross-section, leading both to a reduction in the ratio CSFBH/CSF and an increase in the ratio DM/CSFBH. On looking at Fig. 4 we find that by reducing the ratio CSFBH/CSF and increasing DM/CSFBH we could possibly fit C5 to both postulated trends - that the ratio CSFBH/CSF falls with increasing cluster mass, and the ratio DM/CSFBH is approximately constant. On the other hand, the AGN feedback is more effective in cluster C4 than in C2 - in C4 the CSFBH cross-section is a smaller fraction of the CSF cross-section, whilst in both cases the DM and CSFBH cross-sections are comparable. This can be explained by looking at Fig. 4 - relatively speaking, the AGN feedback has had a greater effect on both the magnitude and slope of the central density profile in cluster C4 as opposed to cluster C2.

It is well known that for an individual cluster the absolute cross-section of a cluster will vary significantly depending on its projection, and we observe this in our clusters. It is also worth pointing out that although a mass trend does appear to be observed in our results, effects of triaxiality and asymmetry effects in clusters could easily mask the true mass trend. As mentioned above, a larger sample of clusters would be required to investigate this point in detail.

## 5 WEAK LENSING RESULTS

In this Section, the results of the analysis of the synthetic weak lensing catalogue are presented, including NFW fits to the data and non-parametric mass maps.

### 5.1 NFW profile fits

COSMOMC (Lewis & Bridle 2002) is used to fit NFW profiles (Navarro et al. 1997) to the simulated weak lensing data, starting outside the strong lensing regime. The NFW profile can be parameterised with a virial radius $r_{200}$, and a concentration parameter $c$. This allows us to define a scale radius $r_s = r_{200}/c$. Inside the virial radius, the mass density of the halo equals $200 \rho_c$, where $\rho_c = \frac{3H_0^2(1+z)}{8\pi G}$ is the critical density of the universe at the redshift of the halo. We may then write the density profile of the NFW model as,

$$
\rho(r) = \frac{\delta_c \rho_c}{(r/r_s) (1 + r/r_s)^3},
$$

where the characteristic overdensity of the halo, $\delta_c$ can be written,

$$
\delta_c = \frac{200}{3} \left[ \frac{c^3}{\ln(1 + c) - c/(1 + c)} \right].
$$

Using the results of Bartelmann (1996) we can write
down the corresponding convergence and shear profiles, which are included in Appendix A.

The probability distribution for the observed galaxy ellipticities, \( p_\epsilon \), can be obtained from the intrinsic ellipticity distribution \( p_\epsilon^i \) (Eq. 13) as follows,

\[
p_\epsilon(\epsilon|g) = p_\epsilon^i(\epsilon^i(\epsilon|g)) \left| \frac{\partial^2 \epsilon^i}{\partial \epsilon^2} \right| = p_\epsilon^i(\epsilon^i(\epsilon|g)) \frac{(|g|^2 - 1)^2}{|\epsilon g^2 - 1|^4} .
\]

Using this, we can compute the log-likelihood function from the probability density for each lensed galaxy, \( p_\epsilon(\epsilon_i) \),

\[
\ell_\gamma = -\sum_{i=1}^{N_\gamma} \ln p_\epsilon(\epsilon_i|\theta_i) ,
\]

which can be evaluated numerically for a trial mass model (with corresponding reduced shear field \( g(\theta) \)) given the lensed ellipticities. The above likelihood calculation is implemented as a module in COSMOMC (Lewis & Bridle 2002), using it as a generic sampler to explore parameter space with the standard Metropolis-Hastings algorithm (Metropolis et al. 1953; Hastings 1970).

The concentrations and virial radii resulting from this analysis are given in Table 2. In clusters C1 and C3, the effect of AGN feedback is to significantly reduce the concentration from the CSF case. In the other clusters, the concentration has still been reduced by the inclusion of AGN feedback, but not as significantly (insofar as the error bars on \( c \) for the two types of physics overlap). In contrast, in all the clusters, the concentrations of the DM clusters are only just below those of the CSFBH clusters. The high concentrations observed for the CSF case are due to the very steep inner density profile of CSF clusters - galaxies closer to the cluster centre contribute comparatively more to the likelihood and thus the MCMC algorithm attempts to fit an
NFW to this very steep inner density region which leads to inflated concentrations.  

As shown in Fig. 6 as is to be expected, the NFW profile is a very poor fit to CSF clusters, due to the large central density spike. The NFW is a better fit to the CSFBH clusters but is still unable to reproduce the density profile in the inner regions of the cluster. At larger radii, the CSFBH and DM profiles converge, at a location dependent on the properties of the cluster. For the more massive clusters that would in practice be studied individually with weak gravitational lensing, that the c and $r_{200}$ values are comparable for the CSFBH and DM simulations bodes well for the study of such dark matter profiles using weak lensing.  

In general, we expect the concentration of the halo to rise as halo mass decreases, and this general trend is observed, with the exception of cluster C3. As noted earlier, in this cluster several dark matter clumps are merging at the cluster centre, and this will reduce the concentration measured using a weak-lensing analysis when fitting a single NFW profile to the entire mass profile.  

5.2 Non-parametric Mass Reconstructions  

The NFW models that we fit to the shear data above are circularly symmetric, and it is clear from Fig. 1 that this assumption of symmetry does not hold for many of the projections. It is also possible to use the simulated weak lensing data to perform non-parametric mass reconstructions of the clusters, which provides complementary information on the detailed structure of the clusters. Non-parametric mass reconstructions use a statistical analysis of many weakly lensed galaxies to identify over-densities in the mass distribution. In this paper, we perform finite-field reconstructions using the algorithm of Seitz & Schneider (1996).  

In Fig. 7 we show mass reconstructions of C5 simulated with CSF, CSFBH and DM. From the Figure we see that the CSFBH and DM clusters are virtually indistinguishable in the mass reconstructions. The CSF cluster shows a higher central density peak in the reconstruction, as expected.  

6 DISCUSSION AND CONCLUSIONS  

In this paper we have investigated the impact of baryonic physics, in particular AGN feedback, on the strong-lensing cross-section of a sample of five simulated clusters. We have also briefly considered their weak-lensing properties.  

Using the cluster simulations of [Puchwein, Sijacki & Springel (2008), the first high-resolution cosmological simulations to include a self-consistent prescription of BH formation and AGN feedback, we have simulated gravitational lensing by clusters with three different physical prescriptions,  

- Dark-matter only (DM)  
- Cooling and star formation (CSF)  
- The above plus AGN feedback (CSFBH)  

We have demonstrated that the inclusion of AGN physics can have a large impact on the lensing properties of clusters by both reducing the strong-lensing cross-section relative to CSF physics, and altering the concentrations measured in a weak-lensing analysis. The principle conclusions of this paper are as follows:  

- Inclusion of baryonic physics can have a dramatic impact on the strong lensing properties of simulated clusters. In CSF simulations we find that the boost in cross-section relative to DM clusters can be significant - our most massive cluster is boosted by a factor of 2-3. The boost is caused by the steepening of the density profile, due to an excess of stars at the cluster centre.  
- We have demonstrated that with the inclusion of AGN feedback, the boost in the cross-section over DM clusters is significantly attenuated relative to those simulations which include only cooling and star formation (CSF). For all but the most massive cluster (C5), where it should be noted that feedback is likely under-predicted, the CSFBH and DM cross-sections are similar. Even for cluster C5, the CSFBH cross-section is $< 2$ times greater than the DM cross-section.  
- The AGN feedback suppresses the build-up of stars and gas in the central regions of clusters, ensuring that the CSFBH inner density slope is shallower than in CSF haloes - this leads to a reduction in the cross-section. The results show some indication for mass dependence of the effect - in more massive clusters the CSF cross-section exceeds the CSFBH cross-section by more, whilst the ratio of CSFBH to DM is approximately constant. To fully investigate this interesting result, a larger sample of clusters is required.  
- We have shown that baryonic physics can have a measurable effect on weak lensing results. The NFW profile is,
as expected, a poor fit to CSF clusters and is not an ideal fit to CSFBH clusters either. Due to the large central density spike of the CSF clusters, measured concentrations can be higher than for the CSFBH and DM clusters. In the mass reconstructions a similar effect is encountered - we see evidence for a prominent central density ‘spike’ in the CSF case.

This work has direct implications for the use of clusters in cosmological parameter estimation. Arc abundance is highly sensitive to baryonic physics, making small samples of clusters difficult to use as a tool for precision cosmology. Rather, for small samples, using lensing to probe cluster properties is a much more fruitful endeavour. In this paper we have demonstrated the sensitivity of cluster lensing properties to the baryonic physics of the cluster, and so if we wish to compare observed arc abundances to those in simulations, we must ensure that the baryons are simulated as accurately as possible. This has important consequences for the interpretation of data from large upcoming surveys. The observational prospects for studies of galaxy clusters are bright: for example DES will contain \( \sim 20,000 \) clusters with mass in excess of \( 2 \times 10^{14} \text{M}_\odot \), up to \( \sim 1000 \) of which could contain strongly lensed arcs. This will also allow for much larger, homogeneously selected, samples of arcs to be obtained.

Aside from the giant arc cross-section considered here, as can be seen from Fig. 3 the DM-only clusters show less substructure than the clusters with baryons, in particular those without AGN feedback. This will influence the appearance of giant arcs that are formed, but also increase the cross-section for the production of smaller separation multiple images by structure outside the critical region of the cluster itself (King 2007).

Our key finding is that with the inclusion of AGN feedback, the addition of baryons to dark-matter haloes boosts the cross-section for the production of arcs by less than previously thought. Clusters simulated with AGN feedback have strong lensing cross-sections that are comparable to those simulated with dark matter only. The inclusion of baryonic physics alone cannot be invoked as a means to increase the arc abundance much beyond that predicted in DM simulations. However, baryonic physics is just one part of a larger physical picture, and a realistic comparison with observed arc abundances would require not only simulation of AGN feedback, but also a realistic source population and the inclusion of large scale structure. This is a topic for future work.

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APPENDIX A: THE CONVERGENCE AND SHEAR OF THE NFW PROFILE

The convergence can be written in terms of a dimensionless radial coordinate \( x = r/r_s \) thus,

\[
\kappa(x) = \kappa_k f(x),
\]

where,

\[
f(x < 1) = \frac{1}{x^2 - 1} \left(1 - \frac{2 \tanh \sqrt{\frac{1-x}{1+x}}}{\sqrt{1-x^2}}\right)
\]

\[
f(x = 1) = \frac{1}{3}
\]

\[
f(x > 1) = \frac{1}{x^2 - 1} \left(1 - \frac{2 \arctan \sqrt{\frac{x-1}{x+1}}}{\sqrt{x^2 - 1}}\right)
\]

and

\[
\kappa_k = \frac{2 \pi f \rho_c}{\Sigma_c}
\]

The shear is given by,

\[
\gamma(x) = \kappa_k j(x),
\]

where,

\[
j(x < 1) = 4 \frac{\tanh \sqrt{\frac{1-x}{1+x}}}{x^2 \sqrt{1-x^2}} + 2 \ln \left(\frac{1}{2}\right) - \frac{1}{x^2 - 1} + 2 \frac{\tanh \sqrt{\frac{1-x}{1+x}}}{(x^2 - 1) \sqrt{1-x^2}}
\]

\[
j(x = 1) = 2 \ln \left(\frac{1}{2}\right) + \frac{5}{3}
\]

\[
j(x > 1) = 4 \frac{\arctan \sqrt{\frac{x-1}{x+1}}}{x^2 \sqrt{x^2 - 1}} + 2 \ln \left(\frac{1}{2}\right) - \frac{1}{x^2 - 1} + 2 \frac{\arctan \sqrt{\frac{x-1}{x+1}}}{(x^2 - 1)^2}
\]

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