A robust argument on the existence of primordial black holes in galactic dark matter halos

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ABSTRACT

If primordial black holes (PBH) within the asteroid/moon-mass range indeed reside in galactic dark matter halos, they must necessarily collide with galactic neutron stars (NS). These collisions must, again necessarily, form light black holes (LBHs) with masses of typical NS, \( M_{LBH} \approx 1.5 \, M_\odot \). LBHs may be behind events already detected by ground-based gravitational-wave detectors (GW170817, GW190425, and others such as a mixed stellar black hole–neutron star mass event GW191219_163120), and most recently by microlensing (OGLE-BLG-2011-0462). Although the status of these observations as containing LBHs is not confirmed, there is no question that gravitational-wave detectors and microlensing are in principle and in practice capable of detecting LBHs. We have calculated the creation rate of LBHs resulting from these light primordial black hole collisions with neutron stars. On this basis, we claim that if improved gravitational-wave detectors and microlensing statistics of the LBH events would indicate that the number of LBHs is significantly lower that what follows from the calculated creation rate, then this would be an unambiguous proof that there is no significant light PBH contribution to the galactic dark matter halos. Otherwise, if observed and calculated numbers of LBHs roughly agree, then the hypothesis of primordial black hole existence gets strong observational support, and in addition their collisions with neutron stars may be considered a natural creation channel for the LBHs, solving the problem of their origin, as it is known that they cannot be a product of standard stellar evolution.

Keywords: black holes – primordial – dark matter – neutron stars

1. INTRODUCTION

A hypothesis that the galactic dark matter (DM) halos may be partially composed of black holes (BHs) of primordial origin (primordial black holes; PBHs) has several fundamental aspects which have been studied by numerous authors, as described, e.g., in the recent reviews by Carr & Kuhnel (2021); Carr et al. (2021); Franciolini et al. (2022). In this Letter we report on one key issue that necessarily arises in the PBH context, namely formation of low-mass black holes (LBHs), that is BHs with masses in the neutron star (NS) mass range \( M_{LBH} \approx 1.5 \, M_\odot \), resulting from collisions of light (asteroid/moon-mass, \( 10^{25} \, g > M_{PBH} > 10^{17} \, g \)) PBHs with NSs. We note here that the abundance of PBHs in this mass range is currently effectively unconstrained.
Abramowicz et al. (2018) (hereafter ABW) have demonstrated, using previous work by Abramowicz et al. (2009) (hereafter ABB), that if light PBHs constitute a non-negligible fraction of galactic DM halos, their existence must have robust and inevitable consequences: they necessarily collide with galactic NSs, nest in their centers, accrete their dense matter interior, and eventually convert the NSs into LBHs, while releasing (possibly) observable electromagnetic (EM) signatures; ABW, in their Eq. 22, estimated the NS→LBH conversion time to be inversely proportional to the initial PBH mass, assuming Bondi accretion approximation, which means that the accretion time may take days or years, depending on \( m \) (see also Richards et al. 2021 for results of numerical calculations).

Various aspects pertaining to the fate of a NS colliding with an asteroid/moon-mass PBH was studied in the past. Fuller et al. (2017) studied the process from the point of view of the r-process nucleosynthesis; specifically, an imploding rotating NS would spin up and shed a part of its mass, estimated to be between 0.1 and 0.5 \( M_{\odot} \). Capela et al. (2013) considered captures of PBHs by NSs in the globular cluster cores, Pani & Loeb (2014) studied energy exchange in the close encounters of PBHs with NSs, with possibly detectable gravitational-wave (GW) emission, while Kainulainen et al. (2021) revisited the ABW’s idea that PBH-NS interaction may be connected with the fast radio burst emission. However, neither of these works put main focus on the fact that the very existence of LBHs would be an actual “smoking gun” evidence for the light PBHs, as the LBHs cannot be created in the standard stellar evolution. A possibility of the LBH formation in the PBH collisions with low-metallicity stars was recently rediscovered by Oncins et al. (2022). LBHs were also directly proposed in the context of recent observations, e.g., Tsai et al. (2021) considered an alternative scenario for the GW170817 event (Abbott et al. 2017), in which one of the components was assumed to be a LBH; such alternative scenario is currently not ruled out by the state-of-art understanding of the multi-messenger physics of the merger (see, e.g., Coughlin & Dietrich 2019).

Inspired by recent discoveries of low-mass compact objects in GWs (Abbott et al. 2021b, lighter component of GW191219_163120 with a mass of \( 1.7^{+0.5}_{-0.6} \) \( M_{\odot} \)) and microlensing observations (Sahu et al. 2022; Lam et al. 2022, lower limit on the mass of the OGLE-2011-BLG-0462 lens estimated to \( 1.6 \) \( M_{\odot} \)), in Section 2 we recast a summary of the ABW arguments, leading to the calculation of the number of the LBH events in Section 3, with a discussion of the potential for breakthrough discoveries by future GW and microlensing observations contained in Sections 3.1 and 3.2, respectively, and conclusions gathered in Section 4.

2. COLLISIONS OF HYPOTHETICAL LIGHT PBH WITH GALACTIC NS

If PBHs exist, they must collide with galactic objects. Single collisions are virtually unobservable, as ABB demonstrated. However, a collision of PBH with NS necessarily initiates observable consequences: a PBH hits NS nearly head on, with impact velocity nearly equal the escape velocity, goes through the NS, loosing a small fraction of its kinetic orbital energy through dynamical friction (Ruderman & Spiegel 1971; Ostriker 1999) and emerges out on the opposite side of the NS with velocity smaller than the escape velocity. This passagebounds a PBH to NS gravitationally. PBH therefore turns back and hits the NS again, loosing orbital energy until it settles at the centre of NS and starts to accrete the NS matter at an increasing rate as its own mass grows. This eventually induces a conversion of the entire NS and formation of an LBH. It is important to stress that this sequence of events – multiple hits, capture in the centre, Bondi accretion, dynamical collapse to LBH – is an unavoidable consequence of fundamental physics, as shown in the ABW paper.

How often do the LBH form? ABW constructed a special purpose population synthesis method to answer this question. The method uses a simplified model of a galaxy consisting of a bulge and a disk, reproducing the density profile required to explain the typically observed galactic velocity profile. The details of the model together with the parameters used are summarized in ABW’s Section 2.2.

Matter content of a model galaxy presented in ABW consists of five species: \( i=1 \) - primordial black holes (PBH), \( i=2 \) - neutron stars (NS), \( i=3 \) - standard stellar mass black holes (BH), \( i=4 \) - low mass black holes (LBH) resulting from the PBH–NS collisions, and \( i=5 \) - stars, interstellar gas and dust. The total local mass density does not change during the galaxy evolution. However, the volume number densities of the species \( n_{(i)}(r) \) do change, as they interact, for example as NS and PBH collide and form together LBH. The evolution of the species \( i=1–4 \) is described by

\[
\frac{\partial n_{(i)}}{\partial t} = \sum_{k=1}^{4} n_{(i)} n_{(k)} C_{(i)(k)} + K_{(i)}, \quad k, i = 1, 2, 3, 4.
\] (1)

Here, the collision coefficients \( C_{(i)(k)} \) express the condition for a direct capture of species \( k \) by species \( i \), and follow from standard argument in classical mechanics based on energy and momentum conservation (it is recalled and explained
in the present context by ABB),

\[ n_{(i)} n_{(k)} C^{(i)(k)} = n_{(i)} n_{(k)} \frac{V^2_{(i)}}{V(r)} R^2_{(i)}. \]  

(2)

Here \( R_{(i)} \) is radius of the \( i \) species and \( V_{(i)} \) the escape velocity from it (it equals to the speed of light \( c \) for the BH species). For \( i = 2, 3 \) the creation coefficients reflect the galactic supernova rate of 0.01 yr\(^{-1}\).

3. CALCULATING THE NUMBER OF LBH EVENTS

The ABW population synthesis method, which we employ here, is based on solving Equation 1, and starts with the initial galaxy state with no NS, BH or LBH. The PBH represent a fraction \( \xi \) of the total gravitating mass in the galaxy, assumed to be \( \sim 7 \times 10^{10} M_\odot \) in the model galaxy. The total number of LBHs derived from the ABW’s model, as a function of characteristic PBH mass \( M_{PBH} \) and mass ratio \( \xi \), is shown in Figure 1. For low \( M_{PBH} \) the curves approach the limit of total number of created NSs, for more heavy PBHs there is an inverse dependence of \( N_{LBH} \) on \( M_{PBH} \).

![Figure 1](image-url)  

**Figure 1.** Absolute number of LBHs in a model galaxy of 13 Gyears age as a function of \( M_{PBH} \) and \( \xi \). Majority of LBHs are created in the galactic bulge. The continuous lines correspond to the total integrated number of LBHs in the galaxy, while the dashed lines represent the LBHs created in the galactic disk.

A number that can be more practical from the observational point of view than the absolute number of LBHs is the ratio of LBHs and NSs numbers. Results of these calculations are shown in Figure 2. The ratio of the number of LBHs and NSs is approximately inversely proportional to \( M_{PBH} \) for a fixed galactic mass PBH fraction \( \xi \), with the model’s simplistic assumption that all PBHs have one characteristic mass \( M_{PBH} \). This example demonstrates that in principle \( N_{LBH}/N_{NS} \) contains information on the \( M_{PBH} \), and therefore can be used to specify the \( M_{PBH} \) mass function, e.g., if all PBHs have small masses, \( M_{PBH} \approx 10^{17} \) g, then the majority of NSs should be converted to LBHs, as \( N_{LBH}/N_{NS} > 1 \). Any observational constraint on the \( N_{LBH}/N_{NS} \) ratio will place limits on masses and abundance of PBHs.

3.1. *Gravitational-wave constraints*

Detections of compact binary inspiral and merger events, including GWs from sources composed of NS-mass components - most notably GW170817, the only one with confirmed EM counterpart, but also GW190425 and "mixed"
BH-NS-mass binaries GW200115, GW191219, GW190917, GW190917, GW190917 (see the GWTC-3 catalogue, Abbott et al. 2021b) – by the LIGO-Virgo-KAGRA (LVK) Collaboration, has revived speculations of the primordial origin of some of the components, due to overall low spin distribution of the observed population and event rates consistent with PBHs Clesse & Garcia-Bellido (2020). Additionally, existence of light PBHs in specific mass ranges is difficult to exclude observationally, see e.g., Carr & Kuhnel (2021); Carr et al. (2021); Franciolini et al. (2022). As estimated in Clesse & García-Bellido (2018), already relatively massive dark compact objects (between $10^{-6}$ and $10^{-5} M_\odot$) could constitute a fraction of DM of order 1%, whereas asteroid/moon-mass PBHs (light PBHs) abundance is effectively unconstrained (Carr & Kuhnel 2021; Carr et al. 2021; Franciolini et al. 2022).

The only EM-bright GW detection so far, the GW170817 event, does not exclude the possibility of one component being a LBH (see e.g., Coughlin & Dietrich 2019). Using the merger rate obtained by the LIGO and Virgo collaborations, based on these recent observations, ABW approximated (see their Section 3.5) the fraction of events containing a LBH to be of the order of a percent of the whole binary merger population containing NS-mass objects.

Clearly, a high signal-to-noise GW measurement which could prove the existence of LBHs would be of a binary LBH insprial and merger, in which component masses $M_1$ and $M_2$ lying well within the NS mass range are measured; if LBHs are created in PBH-induced implosion event, their masses should be systematically lower than the progenitor NS masses due to mass-shedding spin up (Fuller et al. 2017); consequently, their spins should be high, as estimated by ABW (their Section 3.5). Just before the merger a binary LBH system would reach frequencies excluded by NS properties (compactness $M/R$, with $R$ denoting the NS radius, and consequently the equation of state), as the maximum final GW frequency can be estimated as $f_{GW} \approx c^3/(2\sqrt{2}G\pi)/(M_1 + M_2)$ for the case of two BHs (Abbott et al. 2017a).

If both components are LBHs, the best-matched waveform would indicate no measurable mass-weighted average tidal deformability (effective tidal deformability of the binary) $\tilde{\Lambda} = (16/13)((M_1 + 12M_2)M_1^2\Lambda_1 + (1\leftrightarrow 2))/(M_1 + M_2)^5$, with $\Lambda_i = k(2/3)\left(R_i/M_i\right)^5$ denoting individual components’ tidal deformabilities, with $k$ denoting a functional of the equation of state. This effect should be especially evident for component masses near the low end of the NS mass spectrum (i.e. for low compactness $M/R$, high tidal deformability objects). For both LBHs being spacetime curvature objects, no detectable EM emission during and after the merger is expected.

If at least one component is a LBH, at least a sub-population of them should possess a relatively high spin, which in turn should have an detectable influence on the detected waveform, i.e., be measurable by the effective binary spin $\chi_{eff} = (M_1\chi_1 + M_2\chi_2)\hat{L}/(M_1 + M_2)$, with $\chi_i$ individual spins, and $\hat{L}$ is a direction of the system’s orbital momentum (Abbott et al. 2021b). If a GW signal was emitted by a LBH-NS system, the resulting measurement of the tidal deformability $\tilde{\Lambda}$ would place a limit on the NS equation of state, as demonstrated in Haskell et al. (2018), since one of the components’ $\Lambda \equiv 0$, potentially creating a tension with already known features of the equation of state of dense matter. Alternatively, a tidal disruption event or an EM-precursor before the merger would be observed, with

\begin{figure}
\centering
\includegraphics[width=\textwidth]{ratio.png}
\caption{Ratio of LBH and NS densities in a model galaxy of 13 Gy ears age, as a function of $M_{PBH}$ – a characteristic mass of PBHs, for 3 different fractions of PBH in a galactic mass composition $\xi$. This ratio represents the expected ratio of occurrence of collisions of stellar mass BHs with LBHs and stellar mass BHs with NSs. The three panels correspond to galactic disk, bulge, and the total galaxy. For large $\xi$ or light $M_{PBH}$ majority of NSs may become LBHs.}
\end{figure}
details depending on component masses and the equation of state (Neill et al. 2021). For a mixed NS-LBH system, a merger and post-merger evolution, especially from the EM point of view, e.g., the kilonova emission (Li & Paczyński 1998) should be potentially differentiable from a binary NS case (Metzger 2019); from the GW point of view, no long-lasting post-merger GW signal is expected, but rather a prompt collapse to a final BH (the only nearby GW merger so far, GW170817, was too far for the detectors’ sensitivity at that time to give conclusive evidence, Abbott et al. 2017b).

Planned increase in the GW strain sensitivity by a factor \( \approx 1.5 \) of the Advanced LIGO (Aasi et al. 2015) and Advanced Virgo (Acernese et al. 2015) detectors for the O4 observing campaign (with a fourth detector, KAGRA Akutsu et al. 2021, joining the global network) scheduled to start in March 2023\(^1\) promises few times larger sensitive volume and hundreds of new transient GW detections, among them at least a few NS-mass inspiral events (Abbott et al. 2018). In addition, searches for hypothetical sub-solar mass inspirals, which may contain LBHs (Abbott et al. 2021a) and general searches for continuous GWs (e.g. Miller et al. 2021, 2022; Abbott et al. 2022) may provide additional evidence or upper limits for PBHs. Farther future, with 3rd generation detectors, the Einstein Telescope (ET, Punturo et al. 2010) and the Cosmic Explorer (CE, Reitze et al. 2019) will guarantee hundreds of thousands of NS-mass binary inspiral detections per year (Maggiore et al. 2020).

In summary, future GW measurements of coalescing binaries with NS-mass components will contain information pertinent to the inner structure of these objects. Systematic evidence for negligible tidal deformabilities, high spins as well as EM counterparts inconsistent with the standard binary NS scenario would serve as indication for the existence of LBHs, and therefore, indirectly, of PBHs.

### 3.2. Microlensing and X-ray constrains

Gravitational microlensing (Paczyński 1986) can be a useful tool for constraining the population of LBHs. This phenomenon is a result of bending of the light rays of a distant source passing near a lensing object. It depends on the mass of the lensing body and is independent of its luminosity. Thus, microlensing provides an unique opportunity to determine a mass of a single lens, even if it is non-luminous and dark. Indeed, the recent announcements of the discovery of dark black hole mass lens in the gravitational microlensing event OGLE-2011-BLG-0462 (Sahu et al. 2022; Lam et al. 2022) proves that the method is sound and reliable.

In practice a direct mass determination via microlensing is complicated because of a degeneration of the lens mass, geometry of the event and its kinematics. To lift this degeneracy three observables must be measured to derive the lens physical parameters: the Einstein ring crossing time, \( t_E \), microlensing parallax, \( \pi_E \), and angular size of the Einstein ring, \( \Theta_E \); e.g., \( M = \Theta_E / \kappa / \pi_E \) where \( \kappa \) is a constant (Gould 2000a). Only in the very rare cases all three observables can be derived directly from photometry of a single lens microlensing. \( t_E \) is routinely measured for every microlensing event, \( \pi_E \) can be generally derived for long-lasting events (\( t_E > 50 \) days) from a tiny deviation of the observed light curve shape from theoretical one due to the orbital motion of the Earth around the Sun, \( \Theta_E \) – only for high magnification events when the finite source size effects can be measured. Fortunately, the duration of the microlensing events depends on the mass of the lens and in the case of LBH mass range predicted events should last several tens or hundreds days. Thus, in the majority of cases of LBH mass microlensing photometry should provide \( t_E \) and \( \pi_E \).

On the other hand the Einstein ring, \( \Theta_E \), can be measured from an additional effect caused by microlensing – the astrometric microlensing, i.e., the shift of the position of the source star image centroid during the phenomenon. This requires very precise astrometry as the astrometric effects are very small, of the order of a milliarcsec in the case of LBH mass. Thus, the space astrometry (HST, Gaia JWST or future astrometric missions) is required or, for very bright sources, ground based interferometry. OGLE-2011-BLG-0462 was a best example of such a synergy where the ground based photometry, mostly from the OGLE survey (Udalski et al. 2015) was used supplemented with the HST astrometric monitoring of the event. This successful detection proves that the detection of LBHs is in principle possible with the gravitational microlensing method. However, one should remember that the microlensing method can detect dark objects of the LBH masses but it cannot in principle distinguish if the lens is an LBH or NS. Nevertheless, some additional follow-up or all-sky survey observations, e.g., the level of X-ray flux, may allow separating LBH from NS, similarly as in the case of OGLE-2011-BLG-0462 (Mereghetti et al. 2022). Thus, large-scale microlensing hunt for

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\(^1\) 15 June 2022 update of the LVK O4 observing run plans: https://observing.docs.ligo.org/plan/.
LBHs/NS combining photometry and astrometry should be in position to shed some light on the putative population of LBHs.

Microlensing provides statistical constraints on the fraction of the dark objects in the Galactic DM halo as a function of object mass. The early limits from the first generation microlensing surveys conducted in the direction of the LMC yielded an upper limit for the fraction of the LBH mass range objects in the Galactic halo dark matter at about 10% based on OGLE-II and OGLE-III observations (Wyrzykowski et al. 2011). Much more extensive, unpublished yet, analysis based on about 20 years long combined OGLE-III and OGLE-IV dataset indicates, however, even more stringent limit – of about 0.5% (P. Mróz – private communication). In the opposite direction – toward dense stellar regions of the Galactic center – additional contribution from disk dark stellar remnants dominates. It is estimated that about 3% of all observed microlensing events in this direction can be caused by classical NSs and 1% by classical BHs (Gould 2000b). Thus, potential microlensing detection of the LBH mass range objects seems to be feasible. What part of them could be real LBHs and what – regular NSs – remains an open question to be answered when a significant sample of such detections is collected.

4. CONCLUSIONS

Current developments of observational multi-messenger astrophysics (GWs, microlensing, X-ray observations) present a potentially fundamental breakthrough opportunity to scrutinize the hypothesis of light PBHs contributing to the gravitational potentials of galactic DM halos, by indirectly proving their existence by means of the existence of LBHs.

A key point of our argument is that the existence of PBHs in galactic DM halos necessarily implies formation of LBHs, i.e., BHs with NS-mass, as shown by ABB and ABW. What follows, inspirals and mergers of LBHs with standard compact objects (stellar mass BHs and NSs) as well as mergers of binary LBHs would produce transient GWs detectable by the contemporary ground-based detectors (LVK) within a Gpc range (with a greater reach in the future, as the sensitivity of the detectors will increase). On the other hand, Galactic microlensing events involving potential LBHs as gravitational lenses are detectable in practice by optical observatories, and may be inspected by X-ray follow-up observations to reconfirm the BH nature of the lens.

From sufficiently complete statistics of these events – which seems to be a matter of years rather than decades – one will definitely build up evidence to decide for or against these two following, mutually-exclusive possibilities: if the observed number of the LBH events would turn out to be inconsistent with the number calculated on the basis of the population synthesis presented in this paper, then the robust conclusion would be that there are no light (asteroid/moon-mass) PBHs in the galactic DM halos. If, however, the observed number would reasonably agree with the calculated one, this would provide a very strong supporting evidence for the existence of the PBHs.

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