Persistent coherence of quantum superpositions in an optimally doped cuprate revealed by 2D spectroscopy

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Quantum materials displaying intriguing magnetic and electronic properties could be key to the development of future technologies. However, it is poorly understood how the macroscopic behavior emerges in complex materials with strong electronic correlations. While measurements of the dynamics of excited electronic populations have been able to give some insight, they have largely neglected the intricate dynamics of quantum coherence. Here, we apply multidimensional coherent spectroscopy to a prototypical cuprate and report unprecedented coherent dynamics persisting for ~500 fs, originating directly from the quantum superposition of optically excited states separated by 20 to 60 meV. These results reveal that the states in this energy range are correlated with the optically excited states at ~1.5 eV and point to nontrivial interactions between quantum many-body states on the different energy scales. In revealing these dynamics and correlations, we demonstrate that multidimensional coherent spectroscopy can interrogate complex quantum materials in unprecedented ways.

INTRODUCTION

Understanding and controlling the properties of quantum materials is an outstanding challenge for contemporary science and could result in enormous technological returns (1). Quantum many-body materials characterized by strong electronic correlations display a multitude of intriguing phases with unique electric and magnetic features, including the Mott transition, colossal magnetoresistance, topological insulators, and high-temperature superconductivity. These macroscopic properties emerge out of microscopic complexity (2), which is rooted in the competing interactions between the degrees of freedom (DOF) (charge, lattice, spin, orbital, and topology) of a large number of electronic states. The balance between these DOF can be tipped by, for example, photodoping, causing marked changes to the macroscopic properties, for example, turning an insulator into a metal (3).

To address the interactions between the different DOF in the prototypical strongly correlated cuprates, a variety of pump-probe time-resolved experiments have been used (4–7). These measurements have been used to map the dynamics of excited electronic populations and quantify the charge-lattice (8–10) or charge-spin (11) couplings. Oscillations in pump-probe traces are indicative of a coherent response involving low-energy excitations, and there are many examples in the literature of these oscillations in strongly correlated electronic materials (11–13). However, in a typical pump-probe experiment, it is difficult to distinguish between competing signal pathways and identify the origin of the coherent response. In most cases, the oscillations in the pump-probe data arise from dispersive excitation of coherent phonons (14), usually optical phonons. Coherent acoustic phonons, excited by a stress gradient at the sample surface due to the laser absorption, have also been shown to generate oscillations as a result of the probe beam reflecting off the front of the shock wave and interfering with the reflection off the sample surface (15). In addition to phonons, low-energy coherent oscillations can also arise from the inherent order in the system and, thus, provide insight into the dominant interactions. The incoherent dynamics of these low-energy excitations can be obtained by measurements with infrared (IR)/terahertz (THz) pulses (16–18). For example, Matsunaga et al. (16) observed the Higgs amplitude mode in a Bardeen-Cooper-Schrieffer (BCS) superconductor using THz time-domain spectroscopy. On the other hand, Mansart et al. (13) attributed coherent oscillations in pump-probe measurements on a cuprate to coherent oscillations of the Cooper pair condensate. In this case, to make that attribution, the relevant oscillations were extracted from a series of pump-probe measurements, and a number of assumptions were made about the excitation process being impulsive stimulated Raman scattering. While potentially opening the door to new physics, this highlights one of the limitations of pump-probe measurements for revealing coherent dynamics: Many different pathways contribute to the nonlinear signal, and while coherent Raman-like pathways are expected to be present, the signal tends to be dominated by population effects and it is difficult to disentangle the different contributions.

Pump-probe experiments are a subclass of transient four-wave mixing (FWM) techniques that have been used for decades to measure dynamics (4, 17, 19). An FWM experiment on a simple two-level system is generally considered as follows: The first pulse generates a coherent superposition between ground and excited states, and the interaction with the second pulse converts this into a population. The third pulse converts this population into a coherent quantum superposition, which relaxes back to the ground state, emitting the signal. In pump-probe measurements, the first two interactions come from a single pulse—the pump, and the third pulse is the probe. The signal is then emitted in the same direction as the probe, and the interference between them gives the change in probe intensity.

For more complex samples that cannot be described as a two-level system, other pathways become possible. For example, instead of the first two pulses combining to excite a population, they can excite a coherent superposition of closely spaced energy states, in much the

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same manner as a coherent Raman experiment. Single-color transient grating experiments are another subclass of FWM, which has been applied to reveal the quasiparticle diffusion coefficients and scattering rates in YBa$_2$Cu$_3$O$_7$ (20). Like pump-probe experiments, these measurements probe population dynamics.

Other FWM approaches, however, can directly probe the coherent dynamics of quantum superpositions (21). To our knowledge, the measurement of these dynamics in a strongly correlated many-body electronic system has not been previously investigated. Multidimensional coherent spectroscopy (MDCS) (22) is an approach to FWM capable of precisely measuring coherent dynamics. It has been widely applied to semiconductors (23), molecules (24), and proteins (25, 26), where it has enabled detailed understanding of relevant interactions. The key enhancement in MDCS over standard FWM experiments is that the phase of the signal is measured in addition to the amplitude. This is achieved by ensuring that the three excitation pulses are phase locked with each other and with a fourth pulse, the local oscillator (LO), which is overlapped with the signal for heterodyne detection. By recording the phase of the signal, both the real and imaginary parts of the response are simultaneously measured without the need of a Kramers-Kronig transformation.

Through the direct measurement of the phase information in MDCS, it becomes simpler to disentangle different pathways, allowing greater control and insight into the interactions in strongly correlated electronic materials. Pathway-selective MDCS provides additional capability to separate different contributions: By controlling the spectral phase and amplitude of the excitation pulses, one can trigger and probe specific components, or pathways, of the nonlinear response of a material, such as pure quantum-coherent signals (27). Here, we use this approach to selectively excite and probe the dynamics of coherent quantum superpositions of low-energy excitations in a typical cuprate superconductor [La$_{2-x}$Sr$_x$CuO$_4$ (LSCO), $x = 15\%$, $T_c \sim 38 \text{ K}$] in the strange metal phase ($T_{\text{effective}} \sim 50 \text{ K}$). We found coherent dynamics persisting for ~500 fs originating directly from the quantum superposition of optically driven states with energy separation of 20 to 60 meV. Interactions with the third optical pulse reveal the correlation between these low-energy excitations and optically driven states at ~1.5 eV.

**RESULTS AND DISCUSSION**

**Experimental description**

The experiment is described schematically in Fig. 1: The first pulse, with wave vector $k_1$ is spectrally shaped to be centered at 1.575 eV with full width at half maximum (FWHM) of 23 meV and a pulse duration of 80 fs; the second and third pulses, with wave vectors $k_2$ and $k_3$, respectively, are centered at 1.54 eV with an FWHM of 23 meV and a pulse duration of 77 fs, such that there is minimal spectral overlap with the first pulse. The first two pulses, which are set to arrive simultaneously, excite a coherent superposition between states, as indicated by the black oscillating curve in Fig. 1 (D and E). The spectral width of the pulses means that only quantum superpositions between states with energy separations ranging from about 20 to 60 meV will contribute to the measured signal beyond pulse

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**Fig. 1. Experimental scheme.** (A) The geometry of the excitation is such that the three excitation pulses with wave vectors $k_1$, $k_2$, and $k_3$ form three corners of a box with the LO on the fourth corner. The excitation is close to normal to the copper-oxygen plane, and the signal, which is overlapped with the LO, is measured in the reflected direction. (B) The shaped spectrum for each of the excitation pulses and the LO are shown together with the unshaped laser spectrum (black). (C) The convolution of $k_1$ and $k_2$ should determine the range of coherences that can be excited, shown in red. The data from the impulsive response from the sample (black squares) confirm this. (D) The first two nondegenerate pulses are overlapped in time, generating quantum superpositions between states separated by energies dependent on the pulse spectra shown in (C). The third pulse arrives at a controllable time, $t_3$, later and probes the coherent evolution of these superpositions through the emission of the signal (red). (E) Two possible signal pathways are depicted for the case of discrete energy levels. The coherent superpositions that are probed can be excited by two “upward” transitions (pathway 1) or an “up” and “down” transition (pathway 2) similar to a coherent Raman-like process.
overlap (Fig. 1C). This reduces the overall strength of the signal by eliminating the population pathways, which also reduces the noise level (27) and, thus, enhances the signal-to-noise ratio of the coherent response being probed. There are many possible pathways by which these coherences could be excited based on where the optical pulses are being absorbed/emitted to/from (see section S1 and fig. S1). Two such signal pathways are shown in Fig. 1E.

For the purposes of our discussion here, we focus on the state of the system after the first two pulses, at which point the sample is in a coherent quantum superposition of states separated by 20 to 60 meV. The third pulse, with an energy of 1.54 eV and wave vector $k_3$, then interacts with this coherent superposition, leading to the third-order signal emitted in the phase-matched direction $k_s = -k_1 + k_2 + k_3$, with a central energy expected at $\sim 1.505$ eV. The emitted signal is overlapped with the LO and sent to a spectrometer where a spectral interferogram is measured and analyzed to provide the amplitude and phase of the signal. To probe the evolution of the coherent superposition excited by the first two pulses, we scanned the delay between the second and third pulses, $t_2$, and measured the evolution of the signal amplitude and phase. The sample was at a nominal temperature of 12 K, but the high repetition rate of 93 MHz and slow thermal relaxation cause the effective temperature to be higher. As detailed in section S2, we estimate the effective temperature of the sample during the experiments to be $T_{\text{effective}} \sim 50$ K ($T_{\text{effective}} \sim 80$ K) for the nominal temperature $T_{\text{nom}} = 12$ K ($T_{\text{nom}} = 66$ K). This pushes the sample above $T_c$ (–38 K), indicating that we are not sensitive to the formation of the superconducting phase.

**Measurements results**

The real part of the measured signal is shown in Fig. 2A as a function of emission energy and delay time $t_2$; the integrated amplitude of the signal as a function of $t_2$ is shown in Fig. 2B. These show a strong response during pulse overlap and then a signal persisting out to $t_2 \sim 500$ fs, indicating that the quantum superpositions excited by the first two pulses remain coherent over this time scale. At pulse overlap, the peak signal corresponds to $\sim 1500$ signal photons/s, compared with a photon flux of $\sim 4.5 \times 10^{14}$/s for each excitation beam. This signal strength is $\sim 10^5$ times smaller than the signal obtained from broadband measurements on GaAs quantum wells (27). To determine a value for the third-order susceptibility, we need to consider electric field amplitudes and get a value of $\chi^{(3)} \approx 2 \times 10^{-6}$.

The heterodyne detection not only helps to measure such a weak signal but also gives both the amplitude and phase of the signal electric field. As a result, the two-dimensional (2D) plot in Fig. 2A shows oscillations as a function of $t_2$, corresponding to the phase of the coherent superpositions that are excited in LSCO. The frequency of these oscillations appears to change as a function of the emission energy. To gain more insight into this signal, the data were Fourier transformed with respect to $t_2$ to generate the 2D spectrum in Fig. 2D. This 2D spectrum shows a narrow peak elongated along the

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**Fig. 2. Coherent dynamics of the low-energy excitations in LSCO.** The temperature of the sample is $T_{\text{effective}} \sim 50$ K (see section S2), and LSCO is in the strange metal phase. (A) Real part of the spectrally resolved signal as a function of $t_2$; the delay between second and third pulses. The oscillating amplitude originates from the phase evolution of the coherent superposition excited by the first two pulses. The peak signal at pulse overlap corresponds to 1500 photons/s [$\chi^{(3)} \sim 2 \times 10^{-6}$]. (B) The spectrally integrated amplitude plotted as a function of $t_2$ shows the decay of the signal extending beyond 500 fs. The pulses cross-correlation is shown in gray. (C) Window functions used to isolate the response during pulse overlap (as wide as the cross-correlation of the pulses) and the response beyond pulse overlap. (D) The Fourier transform of the data with respect to $t_2$ yields the 2D spectrum, where $E_2$ corresponds to the coherence energy, i.e., the energy difference between the states in the quantum superposition. By windowing the data using the window functions shown in (C), the response at pulse overlap (E) and after pulse overlap (F) can be isolated. In (F), the diagonal peak shape corresponding to the extended signal becomes clear. In the insets of (D) to (F), a cross-diagonal slice of the respective 2D spectrum is plotted.
The 2D spectrum corresponding to the signal persisting beyond pulse overlap (Fig. 2F, obtained by windowing the data with the red function displayed in Fig. 2C), indicates that a signal is generated for a large distribution of coherence energies \((E_2)\) or, in other words, that a broad distribution of low-energy states are coherently excited and contribute to the extended signal. The projection of the data onto the \(E_2\) axis matches closely the distribution of energy differences expected between the first two pulses, as shown in Fig. 1C. For such a large distribution of coherence energies, one would normally expect the macroscopic coherence of the ensemble, and hence the measured signal, to decay rapidly (<50 fs) due to the different frequency components evolving to be out of phase. The expected 2D spectrum would then appear as a broad peak, matching the contribution that arises during pulse overlap (Fig. 2E). However, the results show that right across the distribution of coherence energies, there is a component that remains coherent for over ~500 fs, generating the narrow peak elongated along the diagonal in Fig. 2 (D and F), with a cross-diagonal width of ~9 meV.

The narrow diagonal peak is reminiscent of what is obtained in photon echo measurements, where rephasing of different frequencies allows homogeneous linewidths to be measured even in the presence of inhomogeneous broadening (21). In the present case, however, there is no rephasing, and the ability to observe the coherent evolution of quantum superpositions with a broad distribution of coherence energies is possible only because there is a correlation between the coherence energy \((E_2)\) and the emission energy \((E_3)\). This correlation is also evident in Fig. 2A, where the frequency of the oscillations varies as a function of the emission energy. This is directly mapped onto the 2D spectrum and leads to the narrow diagonal peak in Fig. 2F. The cross-diagonal width of this peak is then determined by the strength of the correlation and/or by the decoherence of the quantum superpositions.

**Comparisons with vibrational coherence and a broad nonresonant response**

To demonstrate that this response is not a typical response, we compare the data to two other samples, one with long-lived discrete vibrational coherences and one with no long-lived coherence. 2D spectra obtained for samples with clear discrete vibrational modes, as is the case for coherent optical phonons, show narrow peaks in \(E_2\), which are spread across a range of \(E_3\) values, as shown in Fig. 3B, for a laser dye molecule. This is typical of the 2D spectra normally expected for this type of experiment and is in stark contrast to what we observed for LSCO. On the basis of the time evolution of the signal amplitude for LSCO (Fig. 2B) and in the absence of the phase information, one would expect a narrow peak along the \(E_2\) axis, similar to those observed for the laser dye (Fig. 3B). With the measurement of the phase information, however, it becomes possible to see the unexpected diagonal line shape for LSCO (Fig. 2F), which reveals the correlation of emission energy and coherence energy over the broad distribution of coherence energies excited.

**Fig. 3. Comparison with vibrational coherences and a broad nonresonant response.** (A) Real part of the signal from IR813 laser dye, as a function of \(E_2\) and \(E_3\). The peak signal at pulse overlap corresponds to \(3.3 \times 10^7\) photons/s \((\chi^{(3)} \sim 2 \times 10^{-4})\). The response extends beyond 1500 fs with several oscillation frequencies. The normalized 2D spectrum (B) and projection on to the \(E_2\) axis (C) show discrete peaks corresponding to the discrete vibrational modes. Here, each peak is broad along the \(E_3\) axis, matching the width of the third pulse. The signal amplitude beyond pulse overlap is about 10× larger for the molecular system (B) than for LSCO (Fig. 2F).

(D) The real part of the signal from an LiNbO\(_3\) crystal as a function of \(E_2\) and \(E_3\) shows the nonresonant response, which decays within the pulse overlap range. The peak amplitude at pulse overlap corresponds to \(1 \times 10^7\) photons per second \((\chi^{(3)} \sim 2 \times 10^{-4})\). The normalized 2D spectrum (E) and projection on to the \(E_2\) axis (F) show broad peaks corresponding to the instrument response function. Further examination of the region beyond pulse overlap is shown in the Supplementary Materials. There is no evidence of any narrow diagonal peak in the nonresonant response.

Without this correlation, a broad distribution of coherences is expected to decay rapidly and within the pulse overlap regime. To confirm this, we repeated these measurements on a lithium niobate crystal. Lithium niobate has a relatively large and spectrally flat third-order nonlinearity, which means that a nonresonant response can be generated under the present excitation conditions. Figure 3D shows the response in the time domain, where the signal decays within the pulse overlap regime. The 2D spectrum (Fig. 3E) shows a broad diagonal peak, as expected for the pulse overlap response and similar to that seen in Fig. 2F for the response in the pulse overlap region for LSCO. The projection of this 2D spectrum onto the \(E_2\) axis (Fig. 3F) reveals the broad distribution of coherences excited (covering the range of 20 to 60 meV). In these measurements, there is no hint of a narrow diagonal peak arising from an extended signal. A closer inspection of the signal beyond the pulse overlap does reveal some extended signal, albeit >10 times smaller than the response at the pulse overlap (compared with ~3 times smaller for the extended response in LSCO). Further transforming the data over this range of delays shows that this response is due to discrete vibration modes in LiNbO\(_3\) (see section S5 for details). There is no indication of any narrow diagonal peak in the 2D spectrum, further confirming that the response we see in LSCO is due to the particular response of LSCO and not due to pulse overlap or any nonresonant response.

**Model**

Traditional analysis of MDCS data uses a perturbative approach to solve the Liouville variant of the Schrodinger equation in a single-particle
framework, with discrete states (28). For strongly correlated materials, such as optimally doped LSCO, the many-body nature of the different excitations and states should be taken into account for a full description and understanding of the experimental results. However, as we show below, a single-particle picture can still qualitatively reproduce the results and provide some physical insight into the correlations of this material. Here, we consider a modified three-level system, where each level is broadened, but the broadening between the top and bottom levels is correlated, as shown in Fig. 4A. After the first two pulses, the coherent superpositions between bands 1 and 2 (indicated by colored dashed arrows) are initiated with a distribution of coherence energies. The third pulse drives the system into a coherent superposition between bands 2 and 3 (black arrow), which radiates to give the signal (colored solid arrows pointing downward), leaving the system in band 2. This pathway is depicted in the Feynman-Liouville diagram in Fig. 4B. This modified three-level system shows how the correlation between the energy of the states in bands 1 and 3 leads to a correlation between the coherence energy, $E_2$, and the emission energy, $E_3$: An increase in coherence energy leads to a decrease in emission energy, and vice versa.

Figure 4 (C to F) shows the result of simulations in this framework, where we have introduced phenomenological decay terms to account for decoherence and relaxation and spectral widths to account for the broadening of the low-energy quantum coherence and the correlation between bands 1 and 3. Full details of the simulations, which are based on standard approaches for MDCS experiments, are given in Materials and Methods. As mentioned earlier, there are at least two factors that can affect the cross-diagonal width of the peak: correlation strength and decoherence (homogeneous linewidth). Thus, there is no unique set of parameters for a given 2D spectrum. In the case of the data in Fig. 4 (C to F), we used a Lorentzian linewidth of 80 meV for the transition between bands 1 and 3, decoherence time of 500 fs for the coherences between bands 1 and 2, and a width for the effective correlation of 4 meV (see Materials and Methods for details). It can be seen that the key experimental features (i.e., the extended signal in $t_2$ and the narrow diagonal peak in the 2D spectrum) are all reproduced in this simplified model. A corollary of the correlations observed is that in the 2D time-domain plot, the signal is shifted to negative times. This is observed in both experiment and simulation and can be described in the framework of “fast-light” (29) or pulse shaping, where a spectral phase gradient is generated by the distribution and evolution of coherence energies as described in section S3.

Signal origin
In conventional superconductivity, electronic excitations are “glued” into Cooper pairs by lattice vibrations (30). It has been suggested that a different kind of glue, for example, involving excitations at low energy, could be responsible for cuprate superconductivity (31). However, understanding the nature of these excitations and the absorption spectrum of the cuprates is puzzling (32). For the nonsuperconducting undoped systems, which appear as shiny metals to the naked eye, the optical absorption is dominated by charge-transfer gap transitions.

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**Fig. 4. Model and simulations for coherent response in LSCO.** (A) The simple single-particle model shows the first two pulses generating quantum superpositions between bands 1 and 2 (dashed colored arrows), with a distribution of coherence energies. The third pulse (solid black vertical arrows) drives the transition to band 3 with energies correlated to those in band 1 (black dotted lines), leading to emission (solid colored arrows), which is anticorrelated with the coherence energy. (B) The corresponding Feynman diagram beginning with the coherent superposition between states in bands 1 and 2 triggered by the first two light-matter interactions. In (C) to (F), we show the results of simulations based on this picture. (C) The evolution of the real part of the signal, (D) the 2D spectrum of the full response, (E) the 2D spectrum from the response during pulse, and (F) the 2D spectrum from contribution making up the extended signal without pulse overlap. The insets show the corresponding cross-diagonal slices.
around 2 eV with a broad, asymmetrical, and long absorption tail, which extends to lower frequencies. When the system is chemically doped, the absorption below ~2 eV increases at the expense of spectral weight above the gap (33): The material develops a Drude peak with a frequency-dependent scattering rate (32) and a broad continuum of excitations extending to low frequency (including the 20 to 60 meV range measured here) with different symmetries (34). Both model calculations (35) and the similarly broad features observed in Raman spectroscopy (36) suggest that this broad continuum involves, in addition to magnetic (37) and vibrational (32, 33) transitions, many-body excitations of different mixed atomic orbitals.

The nature of the low-energy coherent excitations observed here could be any one of these or indeed a combination of one or more (e.g., vibronic states of the correlated many-body system). At this stage, we cannot definitively identify the states with which our laser pulses are interacting; however, we consider some of the possible processes below.

The equilibrium band structure of optimally doped LSCO reveals a continuous density of states from well below the Fermi energy (E_F) level to well above it (38). It is then possible that states from about 1.55 eV (the laser photon energy) below E_F to ~1.55 eV above E_F can be involved in generating the nonlinear signal detected in our multi-dimensional experiment (see section S1 for possible pathways). Previous pump-probe experiments indicate that high-energy optical excitations decay on the tenths of a femtosecond time scale (4, 8), while longer lifetimes have been found by angle-resolved photoemission spectroscopy measurements for excitations around E_F (39). This suggests that the quantum-coherent superpositions that persist for ~500 fs could involve states close to E_F. The first two interactions could then be considered as a coherent Raman-like process where we ignore any resonant interactions involving the first two pulses with higher-energy excitations. This is justified by data taken as a function of the delay between the first two pulses, t_1, and the corresponding 2D spectrum correlating E_1 and E_2, which shows none of the correlations seen in Fig. 2 (see section S4).

Previous Raman measurements on similar samples revealed a smooth, essentially featureless spectrum over the range of E_2 energies probed here (34, 36). Raman modes of different symmetry (primarily A_1g, B_1g, and B_2g) have been identified by polarization controlled experiments, with the two modes with B symmetry (B_1g and B_2g) being of particular interest for their possible role in the pairing mechanism (13). We have repeated our MDCS measurements with different polarization combinations, as shown in Fig. 5. These results reveal little difference between colinear and cocircular excitation, but the peak intensity drops to 50% of the amplitude for cross-circular and ~10% for cross-linear excitation. With the caveat that we expect that the surface stress is minimal in our samples (40), these results are not consistent with the trends expected for a Raman process involving modes with A or B symmetry: for B_1g or B_2g symmetry, one would expect no difference between colinear and cross-linear excitation but complete cancelation of the signal in going from cocircular to cross-linear (34). For acoustic modes with A_1g symmetry, one would expect complete cancelation for both cross-linear and cross-circular polarization sequences (34). These results confirm that while the signal we observe is similar to a simple Raman measurement with nonresonant optical fields, this cannot completely describe the results and the interaction with a higher energy level (band 3 in Fig. 4) is required. Last, regardless of the possible surface stress (40), the signal is strongly suppressed for the cross-linear configuration, suggesting that the excitation triggered by the third pulse should be close to a linear dipole transition, like a charge-transfer excitation.

Recent pump-probe measurements by Miyamoto et al. (11) on the Mott insulator Nd_2CuO_4 showed oscillations with frequency that depends on the probe energy. This trend is similar to what we observe here (Fig. 2F) and may have the same origin. Miyamoto et al. (11) explained these oscillations as polarization beating between different pathways involving two magnon excitations. However, there are some important aspects of the results that are not explained within their model, including the relatively long coherence time/narrow linewidth implied in their measurements and identified here. One of the advantages of MDCS is that it measures the phase of the signal and its evolution, which means the coherent response measured here can only come from quantum superpositions in the sample and not polarization beating. The correlation between the states at low and high energy that we identify here as a result of this phase evolution could also underlie some of the unexpected behavior in the pump-probe results on Nd_2CuO_4 (11). The challenge remains, however, to understand the origin and nature of these correlations.

CONCLUSIONS

Here, we applied MDCS to a prototypical many-body quantum material, LSCO, and found novel quantum signatures: a ~500-fs-long coherent signal originating from the superpositions of many-body states at low energy. We found a strong correlation between the energy of this coherence and the optical energy of the emitted signal, which indicates a coherent interaction between the states at low and high energy in these complex systems.

A fundamental concept valid for correlated electronic materials, which is at odds with single-particle theories, is that when the number of available excitations change by, e.g., chemical substitution (32) or photodoping (3, 6), so too does the band structure (33, 35, 38). Thus, the effective energy structure of the sample can change transiently as the measurement proceeds, which can lead to links between low-energy excitations and optically excited electronic states. We propose that it is these interactions that lead to the correlations that we measure between the coherent quantum superpositions with an
energy of 20 to 60 meV and an optically driven states of ~1.55 eV above this. Beyond the specific interpretations, these results demonstrate that MDCS is a powerful tool to study electronic correlations and opens the door to addressing directly the quantum-coherent states of many-body matter.

**MATERIALS AND METHODS**

**Sample details**

The crystal was grown by using the flux technique. Stochiometric amounts of high-purity (>99.99%) La2O3, SrCO3, and CuO chemicals were mixed. Furthermore, 75 mole percent of CuO was added as flux. These powders were placed in a platinum crucible, covered tightly with a platinum lid, and heated in a chamber furnace. The crucible was heated to 1250°C and kept there for 10 hours, and then it was slowly cooled down to 1100°C at a rate of 2°C/hour. After the growth, the flux was separated by inverting the crucible when it was at 1100°C. Last, the furnace was cooled down to room temperature at the rate of 50°C/hour. (41). The grown crystals were annealed under oxygen flow to increase the Tc and cooled very slowly down to room temperature, so that the strain should be reduced to a minimum. The Sr doping was 0.15, and it was checked by the electron probe microanalysis technique. The magnetic properties were measured using SQUID (superconducting quantum interference device) magnetometry.

**Measurements details**

The transient FWM experiments were performed using the experimental apparatus described previously (27, 42). It uses a Ti:sapphire oscillator generating pulses centered at ~1.55 eV and spectrum shown in Fig. 1B (black) at a repetition rate of 93 MHz. The laser output was compressed using a folded prism compressor and split into the four beams in a box geometry by a beam shaper, consisting of a 2D grating pattern applied to a spatial light modulator (SLM). The four beams were collected by a lens and propagated through all common optics, in a 4F geometry, to ensure a high level of phase stability between all four beams. They were incident on an SLM-based pulse shaper, which allows independent control of the spectral amplitude and phase for each of the four beams. The spectral phase was first optimized to ensure properly compressed pulses by performing spectrally resolved cross-correlations of each pair of pulses. A spectral phase described by a fourth-order polynomial was applied in the SLM pulse shaper, with the coefficients varied to optimize the cross-correlations and minimize the pulse durations. Similar results were obtained by using a dispersion scan approach (43) to optimize the spectral phase on each pulse individually. The pulse duration of the unshaped pulse was 25 fs. The spectral amplitude of the three excitation pulses and LO were shaped to give the spectra shown in Fig. 1B (colored). Cross-correlations of the individual shaped pulses were performed, and spectral phase optimization was repeated to ensure a flat spectral phase. The pulse durations for these shaped pulses were 80 fs (pulse 1) and 77 fs (pulses 2 and 3).

To control the timing of each pulse, and hence the interpulse delays, independent spectral phase gradients were applied to each pulse. The LO was attenuated and delayed by a neutral density filter, and the four beams were focused onto the sample with a 20-cm lens.

The signal generated in the phase-matched direction \(-k_1 + k_2 + k_3\) was spatially overlapped with the LO, which copropagates into a spectrometer where a spectral interferogram is detected, providing details of the signal amplitude and phase. Other signals originating from different wave mixing are emitted in very different directions and were not detected. An eight-step phase cycling procedure was used to isolate the signal from background scatter and enhanced the signal-to-noise ratio.

In the measurements reported here, data were acquired by setting the delay between the first and second pulses to zero \((t_1 = 0)\) and increasing the delay of the third pulse \((t_2)\) by controlling its spectral phase. From this series of interferograms, the time-resolved signal can be obtained as shown in Fig. 2A. Fourier transforms of the data with respect to \(t_2\) lead to the 2D spectra in Fig. 2D–F. The average power in each excitation beam for these experiments was 400 μW. Additional measurements at different intensities were performed to ensure that these experiments were being done in a third-order regime. The linear polarization-dependent experiments were performed by introducing a half-wave plate and linear polarizer into each beam and setting the polarizations accordingly. For the circularly polarized experiments (Fig. 5), an additional quarter-wave plate was introduced after the linear polarizers to convert the linear polarizations to circular polarization. The LSCO samples were mounted in a temperature-controlled recirculating cryostat. Measurements were recorded with the sample temperature nominally at 12 and 66 K and give consistent results, indicating the superconducting phase was thermally melted (see section S2).

The laser polarization was in the copper-oxygen a-b plane of LSCO, and the signal is independent of the sample orientation in the a-b plane (e.g., if the laser fields are parallel, perpendicular, or in between a and b).

**Simulation**

We simulated the nonlinear response of LSCO by numerically solving the Liouville variant of the Schrödinger equation for the three-level system described in Fig. 4 (A and B)

\[ i\hbar \rho = [H, \rho] \]

with

\[ H = H_0 + H_{\text{int}} + H_{\text{relax}} \]

\[ H_0 = \begin{bmatrix} \epsilon_1 & 0 & 0 \\ 0 & \epsilon_2 & 0 \\ 0 & 0 & \epsilon_3 \end{bmatrix}, \]

\[ H_{\text{int}} = \begin{bmatrix} 0 & 0 & E(\mathbf{k}, t)\mu_{13} \\ 0 & 0 & E(\mathbf{k}, t)\mu_{23} \end{bmatrix} \]

\[ [H_{\text{relax}}, \rho] = -i\hbar \gamma_{ij} \rho_{ij} \]

where \(\epsilon_i\) is the energy of state \(i\); \(\mu_{ij}\) is the transition dipole moment for the transition between state \(i\) and \(j\); and \(\gamma_{ij}\) is the phenomenological decay rate for each term in the density matrix, \(\rho_{ij}\), which corresponds to a population lifetime \(t_i\). The rotating wave approximation was made, and the electric field of the excitation pulses, \(E(\mathbf{k}, t)\), is given by

\[ E(\mathbf{k}, t) = E_1(t) e^{i(\mathbf{k}_1 r - \omega_1 t)} + E_2(t) e^{i(\mathbf{k}_2 r - \omega_2 t)} + E_3(t) e^{i(\mathbf{k}_3 r - \omega_3 t)} \]

where \(k_i\) is the wave vector, \(\omega_i\) the frequency, and \(E_i(t)\) is the real valued Gaussian envelope function of pulse \(i\), with width given by the experimental pulse durations. The electric field was treated perturbatively, and the system of equations was expanded up to third order, with the emitted signal being proportional to the third-order polarization, corresponding to \(\mu_{13}\rho_{13}\), with wavevector \(-\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3\). The resultant set of interdependent differential equations was numerically solved to facilitate the use of realistic pulses with finite duration.
We took the dipole moment for the transition between states 1 and 3 ($\mu_{13}$) to be the same as the one between states 2 and 3 ($\mu_{23}$). The homogeneous linewidths of these transitions ($\gamma_{13}$ and $\gamma_{23}$) were set to 80 meV, such that the $\sim 1.55$-eV coherent superpositions decay within the pulse duration, as observed in the projection of the 3D spectrum onto the one-quantum 2D spectrum shown in fig. S4. The homogeneous linewidth $\gamma_{12}$ of the zero-quantum coherence transition was set to 8 meV, corresponding to a decay time of 500 fs. The energies of states 1 and 3 were kept fixed at 0 and 1.54 eV, and to account for the distribution of coherence energies, the simulation was run for different values of $\epsilon_{t}$ and the results were summed, weighted by a Gaussian distribution centered at 40 meV with 40-meV FWHM. By varying the energy of state 2, the energy differences between 1 and 2 and between 2 and 3 were anticorrelated, as described in Fig. 4A, and observed in the experiments. The strength of the correlation between bands 1 and 3 was controlled by adjusting the effective spectral width of the third pulse, which drives the transition indicated by the black line in Fig. 4A. For the data shown in Fig. 4E, corresponding to the case where the long-lived coherences were observed, this width was set to 4 meV. For Fig. 4D, where the pulse overlap regime is simulated, this width was set to 30 meV, and between 1 and 2 and between 2 and 3 were anticorrelated, as described in Fig. 4C, the sum of these two contributions was plotted.

SUPPLEMENTARY MATERIALS
Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/6/9/eaaw9932/DC1
Section S1. Possible pathways for excitation of the 40 ± 20–meV coherent superpositions
Section S2. Heating effects due to laser excitation
Section S3. Emission at negative times
Section S4. Correlations between $E_{1}$, $E_{2}$, and $E_{3}$
Section S5. Response from LiNbO$_3$
Fig. S1. Signal pathways.
Fig. S2. Thermal effects.
Fig. S3. Apparent signal at negative delays.
Fig. S4. 3D spectra from LSCO and projection onto the 2D planes.
Fig. S5. Windowed 2D spectra from LiNbO$_3$
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