A new variant of the effective pomeron exchange model is proposed for the description of the correlation, observed in \( pp \) and \( p\bar{p} \) collisions at center-of-mass energy from SPS to LHC, between mean transverse momentum and charged particles multiplicity. The model is based on the Regge-Gribov approach. Smooth logarithmic growth with the collision energy was established for the parameter \( k \), the mean rapidity density of charged particles produced by a single string. It was obtained in the model by the fitting of the available experimental data on charged particles rapidity density in \( pp \) and \( p\bar{p} \) collisions. The main effect of the model, a gradual onset of string collectivity with the growth of collision energy, is accounted by a free parameter \( \beta \) that is responsible in an effective way for the string fusion phenomenon. Another free parameter, \( \tau \), is used to define string tension. We extract parameters \( \beta \) and \( \tau \) from the available experimental results on \( \langle p_t \rangle \)-multiplicity correlation at nucleon collision energy \( \sqrt{s} \) from 17 GeV to 7 TeV. Smooth dependence of both \( \beta \) and \( \tau \) on energy allows to make predictions for the correlation behavior at the collision energy of 14 TeV. The indications to the string interaction effects in high multiplicity events in \( pp \) collisions at the LHC energies are also discussed.

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1. Introduction

The correlations between mean transverse momentum and charged multiplicity ($\langle p_t \rangle$-$N_{ch}$ correlations) in hadron collisions have been observed and measured at wide range of energy from SPS to the LHC [1–9]. A number of non-trivial effects that were observed, among them the are general growth and “flattening” of charged particles $p_t$ values with the event complexity and the increase of mean $p_t$ with the collision energy, could be explained in terms of some collective processes (such as string fusion, color reconnection, flow etc.), that are relevant also in AA interaction.

In this connection the understanding of the $pp$ collisions at the LHC is important as a base for the analysis of heavy-ion results.

In the present work we develop further the extended multi-pomeron exchange model proposed earlier in [10] for analysis of $\langle p_t \rangle$-$N_{ch}$ correlations in $pp$ and $p\bar{p}$ collisions. The model is based on the Regge-Gribov approach, with an effective introduction of the string collectivity effects, performed in a way, similar to [10]. But, contrary to [10], we manage to reduce the number of actually free parameters to only two, that are relevant to string collectivity and string tension. This is achieved, in particular, by establishing a smooth logarithmic growth with the collision energy of the mean rapidity density of charged particles produced by a single string. Below we present the details of the extended multi-pomeron exchange model followed by the new analysis of available data on $\langle p_t \rangle$-$N_{ch}$ correlations in $pp$ and $p\bar{p}$ collisions.

2. Extended effective multi-pomeron exchange model

In constructing of the model for $pp$ or $p\bar{p}$ collisions we start from the probability of the event with $n$ cut-pomeron exchanges [11, 12]:

$$w_n = \sigma_n / \sum_{n'} \sigma_{n'} , \quad (2.1)$$

where $\sigma_n$ is the cross section of $n$ cut-pomeron exchange:

$$\sigma_n = \frac{\sigma_P}{n^2} \left( 1 - e^{-z} \sum_{l=0}^{n-1} \frac{z^l}{l!} \right) , \quad z = \frac{2C\gamma s^\Delta}{R^2 + \alpha' \log(s)} \quad (2.2)$$

The numerical values of the parameters used are the following [13]:

$$\Delta = 0.139, \quad \alpha' = 0.21 \text{ GeV}^{-2}, \quad \gamma = 1.77 \text{ GeV}^{-2}, \quad R_0^2 = 3.18 \text{ GeV}^{-2}, \quad C = 1.5 .$$

Using probabilities (2.1) we can calculate mean and variance of the number of cut-pomerons:

$$\langle n \rangle = \sum_{n'=0}^\infty n' w_{n'} , \quad \text{Var} n = \sum_{n'=0}^\infty n'^2 w_{n'} - \langle n \rangle^2 .$$

The results are plotted in Fig. 1 as a function of collision energy $\sqrt{s}$.

For the description of the charged multiplicity we assume that each cut-pomeron corresponds to a pair of strings, each of them emits particles into given acceptance according to Poisson distribution with mean value, proportional to this (pseudo)-rapidity interval. Therefore the probability for $n$ cut-pomerons to produce $N_{ch}$ particles is given by:

$$2$$
Figure 1: Mean (solid line) and variance (dashed line) of the number of pomerons.

\[ P(n, N_{ch}) = \exp(-2nk\delta) \frac{(2nk\delta)^{N_{ch}}}{N_{ch}!}, \quad (2.3) \]

where \( k \) is the mean multiplicity per rapidity unit from one string, \( \delta \) is the acceptance i.e. width of (pseudo-)rapidity interval.

Using formula (2.3) we obtain the probability to have \( N_{ch} \) particles in a given event:

\[ \mathcal{P}(N_{ch}) = \sum_{n=1}^{\infty} w_n P(n, N_{ch}) \]

and mean charged multiplicity:

\[ \langle N_{ch} \rangle = \sum_{N_{ch}=0}^{\infty} N_{ch} \mathcal{P}(N_{ch}). \quad (2.4) \]

For the description of pseudorapidity density of charged particles we can use formula (2.4), substituting \( \delta = 1 \). Note, that in this case we have only one parameter \( k \) to adjust for the description of experimental data.

In order to cover also the transverse momentum and its correlation with multiplicity, the extension of the model is performed as follows. We use the general idea of the Schwinger mechanism of particles production from one string [14], that the transverse momentum distribution of charged particles from a string has a Gaussian form:

\[ \frac{d^2 N_{ch}}{dp_t^2} \sim \exp \left( -\frac{\pi (p_t^2 + m^2)}{\tau} \right), \quad (2.5) \]

where \( \tau \) corresponds to the string tension.

The assumptions that all strings are identical or that the string tension does not depend on multiplicity would give zero correlation between transverse momentum and multiplicity. In order to include collectivity in our model and to be able to describe non-trivial \( \langle p_t \rangle - N_{ch} \) correlations we introduce, similar to [10], the new parameter \( \beta \), which is responsible in an effective way for string interaction (fusion), with \( \beta = 0 \) corresponding to the absence of collective effects. Thus the dependence of transverse momentum from one string on the number of cut-pomerons is introduced:

\[ \frac{d^2 N_{ch}}{dp_t^2} \sim \exp \left( -\frac{\pi (p_t^2 + m^2)}{n^\beta \tau} \right), \quad (2.6) \]

Note that denominator in (2.6) gives effective string tension \( n^\beta \tau \).
The pseudorapidity density of multiplicity as a function on energy. Experimental data are borrowed from [15].

The values of the parameters $\beta$ and $t$ are obtained using the data on $(p_t)_{N_{ch}}$ correlations from 17 GeV to 7 TeV. Results of fitting are shown in Fig. 4. Parameters $\beta$ and $t$ as function on energy are shown in Fig. 5. The smooth behaviour of parameter $\beta$ with energy is obtained and approximated in Fig. 5 by $\beta = 1.16[1 - (\ln \sqrt{s} - 2.52)^{-0.19}]$. Similar to [10] the set of obtained variables $t$ have split into two subsets: one is around $t = 0.566 \text{ GeV}^2$ and the second $t = 0.428 \text{ GeV}^2$. This discrepancy
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**Figure 4:** Experimental data [1–9], fitted by the present model.
between them may be related to differences in data analysis procedures and interpolation to the softest part of $p_t$ spectra, performed by various experiments. The points belonging to the first subset are used for the further analysis because they provide the correct values of $\langle p_t \rangle$ (see [10]).

3.1 Predictions for the LHC at 14 TeV.

Using obtained dependence of the parameters $(k, \beta, t)$ on energy we extrapolated their values up to the energy $\sqrt{s} = 14$ TeV and calculated the $\langle p_t \rangle$-$N_{\text{ch}}$ correlation function. For the parameter $t$ we used three assumptions: no dependence on energy ($t = 0.566$ GeV$^2$), parabolic fit ($t = 0.731$ GeV$^2$) and $t = 0.676$ GeV$^2$ – the same as at 7 TeV. The results are shown in Fig. 6. The experimental data at this energy would enable to make final decision concerning the behaviour of $t$ with energy.

3.2 Discussion of the possible relation to the string fusion

The parameters, obtained after the fitting procedure, demonstrate a growth of multiplicity from one string ($k$) with increasing energy, accompanied by an increase of transverse momentum. This result agrees with the basic concept of string fusion model [16, 17], according to which at high energies strings with greater tension are formed due to the overlap in the transverse plane. In line with this model, the average multiplicity per rapidity unit and mean square of the transverse momentum of charged particles from a cluster of fused strings are proportional to the square root of energy.

![Figure 5: Dependence of parameters $\beta$ (left) and $t$ (right) on energy.](image1)

![Figure 6: Predictions for the $\langle p_t \rangle$-$N_{\text{ch}}$ correlation function at 14 TeV, obtained for $|\eta| < 2.4$.](image2)

![Figure 7: Ratio of mean multiplicity from one source over characteristic $p_t$ from one source.](image3)
of the number of strings overlapping: \( \mu = \mu_0 \sqrt{\eta}, p_t^2 = p_0^2 \sqrt{\eta} \). Thus, the ratio of these quantities in average should not depend on energy: \( \frac{\mu}{p_t^2} = \frac{\mu_0}{p_0^2} \).

Since in our model the product \( \langle n \rangle^{\beta t} \) is a characteristic square of the transverse momentum of the particles from one source, fulfillment of this condition can be checked by plotting the ratio \( k / (\langle n \rangle^{\beta t}) \) as a function of energy. The results presented in Fig. 7 indeed show no dependence of this ratio on energy. Thus, we can conclude that the experimental data support the hypothesis of the string fusion as the source of collectivity in \( pp \) and \( p\bar{p} \) collisions in a wide energy range.

4. Conclusions

The extended multi-pomeron exchange model with collectivity effects is applied to the analysis of experimental data on \( \langle p_t \rangle - N_{ch} \) correlation in a wide energy range of \( pp \) and \( p\bar{p} \) collisions. Thus it was possible to establish:

(i) Smooth logarithmic growth with the collision energy of mean multiplicity \( k \) of charged particles from one string;

(ii) Smooth growth of the string collectivity parameter \( \beta \) with the collision energy;

(iii) Stability of the string tension parameter \( t \), which is consistent with a constant.

Results are pointing at the numerical agreement with string fusion model. Predictions for \( \langle p_t \rangle - N_{ch} \) correlations at the future LHC collision energy of 14 TeV were obtained.

References

[1] T. Anticic et al. (NA49 Collab.), Phys. Rev. C 70 (2004) 034902.
[2] C. De Marzo et al., Phys. Rev. D 29 (1984) 363.
[3] V. V. Aivazyan et al., Phys. Lett. B 209 (1988) 103.
[4] A. Breakstone et al. (ABCDHW Collab.), Phys. Lett. B 132 (1983) 463.
[5] C. Albajar et al., Nucl. Phys. B 335 (1990) 261.
[6] G. Arnison et al. (UA1 Collab.), Phys. Lett. B 118 (1982) 167.
[7] F. Abe et al., Phys. Rev. Lett. 61 (1988) 1819.
[8] T. Alexopoulos et al., Phys. Lett. B 336 (1994) 599.
[9] V. Khachatryan et al. (CMS Collab.), JHEP 1101 (2011) 079.
[10] N. Armesto, D. A. Derkach, G. A. Feofilov, Phys. Atom. Nucl. 71 (2008), 2087.
[11] A. B. Kaidalov, Phys. Lett. B 116 (1982) 459.
[12] A. B. Kaidalov and K. A. Ter-Martirosyan, Phys. Lett. B 117 (1982) 247.
[13] I. A. Lakomov, V. V. Vechernin, PoS (Baldin ISHEPP XXI) 072 (2012).
[14] J. Schwinger, Phys. Rev. 82 (1951) 664.
[15] B. Abelev, et al. (ALICE Collab.), Phys. Rev. Lett. 110 (2013) 032301.
[16] M. A. Braun, C. Pajares, Nucl. Phys. B 390 (1993) 542.
[17] M. A. Braun, R. S. Kolevatov, C. Pajares, V. V. Vechernin, Eur. Phys. J. C 32 (2004) 535.