All-optical generation of antiferromagnetic magnon currents via the magnon circular photogalvanic effect

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We introduce the magnon circular photogalvanic effect enabled by two-magnon Raman scattering. This provides an all-optical pathway to the generation of directed magnon currents with circularly polarized light in honeycomb antiferromagnetic insulators. The effect is the leading order contribution to magnon photocurrent generation via optical fields. Control of the magnon current by the polarization and angle of incidence of the laser is demonstrated. Experimental detection by sizable inverse spin Hall voltages in platinum contacts is proposed.

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The creation and control of spin currents at the nanoscale are key goals in spintronics and magnonics [1]. The recent synthesis of quasi-two-dimensional layered magnetic insulators, such as transition-metal phosphorous trichalcogenides $MPX_3$ ($M = \text{Ni, Mn, Fe and } X = \text{S, Se}$) and chromium trihalides $\text{CrX}_3$ ($X = \text{Cl, I, Br}$) with a band gap of $\sim 1$ eV [2–8] is inspiring ideas on how to employ such materials in future spintronics devices [9,10]. One of the most promising approaches is to use optical means for spin current generation and control [11,12]. Importantly, this would allow one to adapt concepts from photocurrent generation in electronic systems, in particular, the circular photogalvanic effect (CGPE). The CPGE holds great promise for functionality and applications since it allows one to selectively generate currents and probe wave-function quantum geometry only on the surface, as demonstrated in 3D [13] and 2D topological insulators [14] as well as Weyl materials [15]. On the other hand, the optical control of magnetization is naturally extended into the ultrafast (THz or faster) regime, as has been demonstrated by coherent control of magnetism in pump-probe experiments [16–23]. The prospects of combining the expertise from CPGE and ultrafast magnetism research with antiferromagnetic spintronics and optospintronics would pave the way toward the next generation of ultrafast optospintronics research with functionality and devices on the horizon. However, there are a number of obstacles to overcome. One of them is the theoretical foundation behind such an approach.

Here we lay the groundwork for an all-optical route to create directed magnon currents in magnetic insulators through the magnon circular photogalvanic effect (MCPGE) enabled by two-magnon Raman scattering. We show that a circularly polarized laser drive generates a magnon current whose strength and direction are controllable through the angle of incidence and polarization via the MCPGE. This magnonic photocurrent is predicted to lead to an inverse spin Hall voltage of experimentally accessible values in platinum contacts, with a characteristic angle dependence, enabling the experimental verification of both the magnon current generation and the underlying MCPGE with existing technology.

The MCPGE as proposed in this paper is the leading contribution [24] to magnon photocurrents in antiferromagnetic insulators. Earlier works have considered the direct coupling of the laser field and the spins via the Zeeman interaction, which is only dominant in the GHz regime and on resonance [25–27]. In contrast, the two-magnon Raman process couples the electric field of the laser to the spins via the same kinetic processes that give rise to the antiferromagnetic exchange interaction, which is ubiquitous in real materials and gives the leading order contribution to the magnon current for optical fields. Since the electric field is stronger than the magnetic field by a factor $c$ (with $c$ the speed of light), it gives an enhancement of the magnon current on the order of $c^2$. Further, since the Raman process creates pairs of magnons with opposite and finite momenta (over the full Brillouin zone), the excitation cross section greatly exceeds that of resonant processes only exciting the system around $\Gamma$. These two-magnon processes also dominate over single-magnon Raman processes enabled by spin-orbit interaction [24,28].
In what follows, we study the generation of magnon currents via two-magnon Raman scattering specifically in collinear honeycomb antiferromagnets. However, the analysis presented below can be straightforwardly extended to general magnetic point groups. We find that the magnon current is determined by the MCPGE and given by

\[ (J) = \zeta \text{Im}(\sigma) \cos \theta \sin^2 \theta (\sin 2\phi \hat{e}_y - \cos 2\phi \hat{e}_x), \]  

(1)

where \( \sigma \) is the nonzero element of the optical susceptibility and \( \theta \) and \( \phi \) determine the propagation direction of the light as shown in Fig. 2. Here, the \( z \) axis coincides with the Néel vector of the system. For subgap excitations, the susceptibility only shows a weak frequency dependence and in the following we assume \( \hbar \omega = 1 \text{ eV} \). The magnitude of \( (J) \) is controlled by the angle of incidence \( \theta \), while its direction is determined by the polar angle \( \phi \) and the chirality \( \zeta \) of the laser. The current vanishes at normal and in-plane incidence, and its direction rotates in the substrate plane with a period \( 2\phi \) as illustrated by the flower shape in Fig. 2(c). Figures 2(a) and 2(b) show the \( y \) component of the current as a function of \( \theta \) and \( \phi \), for a laser with left- or right-handed polarization, respectively. The results clearly illustrate the direct proportionality of \( (J) \) to the chirality of the laser and how the current can be controlled via the MCPGE.

The expression for the magnon current \( (J) \) can be understood from a symmetry analysis of the system. The light-matter coupling due to Raman scattering is quadratic in the electric fields [24,29,30], which in line with previous work gives a quadratic dependence of the current on the incident electric field [13–15,31]. Since the magnon photocurrent is obtained by expanding the optical susceptibility to lowest order in the Raman interaction, only odd orders will contribute. The third order susceptibility vanishes by symmetry, and hence the leading order contribution comes from the fifth-order tensor \( \alpha_{ijklm} \). For a collinear Neél state, the system has \( C_{3v} \) symmetry and the susceptibility has to be invariant under the corresponding symmetry transformations. The \( C_{3v} \) and index permutation symmetries reduce the original 32 elements of \( \alpha_{ijklm} \) to 16 nonzero elements, out of which three are independent [32]. Among these, only one corresponds to a process of net angular momentum transfer that can generate a nonzero magnon current, leading to Eq. (1).

In a typical experiment, the sample and angle of incidence are held fixed while the polarization is varied via a quarter wave plate. Therefore, we show in Fig. 3(a) the magnon photocurrent as a function of polarization for a given configuration \((\theta, \phi)\). The current is maximal for circular polarization. The current is normalized to the maximal value \( J_{\text{max}} \) obtained at \( \theta \approx 55^\circ \) and \( \phi = 45^\circ \). The horizontal grid lines indicate where the incident field is parallel to the \( x \) or \( y \) axis. (c) The \( x \) component (orange) and \( y \) component (black) of the magnon photocurrent as a function of polar angle \( \phi \). (d) Illustration of the proposed experimental setup with a honeycomb antiferromagnet and metallic contacts (Pt) for magnon current readout. In all panels, the model parameters are \( S = 5/2, J_1 = 1.54 \text{ meV}, J_2 = -0.14 \text{ meV}, J_3 = 0.3 \text{ meV}, J_4 = 8.6 \mu \text{eV}, \) and \( B = 0 \), as appropriate for MnPS_3 [36,37].

![FIG. 1. Magnon photocurrent via two-magnon Raman scattering. (a) The magnetic unit cell with the vectors \( \delta^n_i \) connecting the \( n \)-th-nearest neighbors. (b) Scattering of right-handed (left-handed) photons into left-handed (right-handed) photons imparting spin angular momentum and creating a magnon pair with zero net momentum carrying a net spin angular momentum current of \( 2\hbar \).](image)

![FIG. 2. Photoinduced magnon current. (a), (b) Photoinduced magnon current along the \( y \) axis as a function of incidence and polar angles \( \theta \) and \( \phi \) for left-handed (a) and right-handed (b) circular polarization. The current is normalized to the maximal value \( J_{\text{max}} \) obtained at \( \theta \approx 55^\circ \) and \( \phi = 45^\circ \). The horizontal grid lines indicate where the incident field is parallel to the \( x \) or \( y \) axis. (c) The \( x \) component (orange) and \( y \) component (black) of the magnon photocurrent as a function of polar angle \( \phi \). (d) Illustration of the proposed experimental setup with a honeycomb antiferromagnet and metallic contacts (Pt) for magnon current readout. In all panels, the model parameters are \( S = 5/2, J_1 = 1.54 \text{ meV}, J_2 = -0.14 \text{ meV}, J_3 = 0.3 \text{ meV}, J_4 = 8.6 \mu \text{eV}, \) and \( B = 0 \), as appropriate for MnPS_3 [36,37].](image)

![FIG. 3. Experimental signatures. (a) Magnon photocurrent as a function of polarization obtained by varying the angle between the electric field of a linearly polarized laser and the fast axis of a quarter wave plate. The resulting polarization is indicated below the quarter wave plate. Therefore, we show in Fig. 3(a) the magnon photocurrent as a function of polarization for a given configuration \((\theta, \phi)\). The current is maximal for circular polarization. (b) Inverse spin Hall effect voltage \( V_{\text{SSHE}} \) induced by a magnon current as a function of temperature \( T \). The main panel shows the diagonal Stokes component, while the inset shows the off-diagonal Stokes (blue, dotted), and diagonal (green, dashed) and off-diagonal (brown, dot-dashed) anti-Stokes contributions to \( V_{\text{SSHE}} \). In both panels, the parameters are the same as in Fig. 2.](image)
polarization and gradually reverses its direction when the polarization is tuned from left to right handed. Incidentally, we find that the current vanishes for linear polarization. The necessity for circularly polarized light can be understood from the requirement of angular momentum conservation, as indicated in Fig. 1: Due to the threefold rotation symmetry of the honeycomb lattice, angular momentum is conserved modulo $3\hbar$. Since each magnon pair generated through Raman scattering carries $2\hbar$ spin angular momentum, the excitation process requires a flip of the photon helicity contributing $\hbar$ to the total angular momentum.

The magnon current can be detected via the inverse spin Hall effect (ISHE) using the setup proposed in Fig. 2: A magnon current generated in the bulk antiferromagnet propagates toward the Pt contacts, where the resulting magnon accumulation is converted into a spin current. The spin current in turn generates a charge current via the ISHE, which induces a voltage $V_{\text{ISHE}}$ [38,39]. Following the discussion in Refs. [40,41], we convert the magnon photocurrent into the signals detected from DC magnon currents launched via the ISHE [42]. Figure 3(b) shows that the current decays rapidly with temperature, and is effectively zero for $T \approx 30$ K. This is in line with experiments on MnPS$_3$ [43], where the magnon current was found to vanish above $T \approx 30$ K, far below the Neel temperature $T_N \approx 80$ K.

The symmetry analysis of collinear honeycomb antiferromagnets shows the generality of a nonzero magnon current generated by the MCPGE, independent of the specifics of the underlying spin Hamiltonian. This indicates that the mechanism is a generic feature of a large class of materials, which should favor an experimental verification. In what follows, we derive Eq. (1) from a concrete microscopic spin Hamiltonian.

The magnetic structure of a collinear honeycomb antiferromagnet is described by the Hamiltonian

$$H = \sum_{(ij)} J_{ij} S_i \cdot S_j + J_c \sum_{(ij)} S_i^z S_j^z - g\mu_B B_0 \cdot \sum_i S_i^z,$$  

(2)

where $J_{ij}$ are bilinear exchange interactions, $J_c$ is an easy-axis anisotropy, and $B_0 = B_0 \hat{z}$ is an external magnetic field along the easy axis. The ground state is approximately given by the Neel state with spins on sublattice A (B) pointing in the positive (negative) $z$ direction. This model is appropriate for van der Waals materials like MnPS$_3$ in the monolayer or weak interlayer coupling limit [36,44-46]. Equation (2) can be augmented by including Dzyaloshinskii-Moriya interactions (DMI). Interestingly, we find that the MCPGE is independent of the DMI.

The low-energy excitations of $H$ to lowest order in $1/S$ are found by Holstein-Primakoff linear spin-wave theory. Transforming to Fourier space, the Hamiltonian is

$$H = \sum_k \Psi_k^\dagger H_k \Psi_k,$$

where $\Psi_k = (a_k^\dagger, \beta_{-k})$ is a Nambu spinor, $H_k = h_0 \mathbf{1} + \hbar \mathbf{r} \cdot \mathbf{t}$, and $\mathbf{r}$ is the vector of third-nearest neighbors, the components of the Hamiltonian are given by

$$h_0 = J + 2J_2 \sum \cos(\mathbf{k} \cdot \delta(2)),$$

$$h_{\pm} = \frac{1}{2} \sum (J_1 e^{-\mathbf{k} \cdot \delta(1)} + J_3 e^{-\mathbf{k} \cdot \delta(3)}),$$

and $h = B/\mathcal{S}$, where $J = 3J_f - 6J_2 + 3J_3$, $J_f = g\mu_B B_0$, and $\delta(\alpha)$ are the vectors between $n$th-nearest neighbors. The Hamiltonian is diagonalized via a paraunitary matrix $U_k$ giving $H = \sum_k \epsilon_{ak} a_k^\dagger a_k + \epsilon_{\beta k} \beta_{-k}^\dagger \beta_{-k}$. Here $\epsilon_{ak/\beta k} \equiv 0 \mp \hbar$, is the dispersion of the upper and lower magnon branches, respectively, and $d = (h_0^2 - h_+^2 - h_-^2)^{1/2}$.

We note that the magnon Hamiltonian is invariant under the combined symmetry $\mathcal{T} \Omega$, where $\mathcal{T}$ is the time-reversal operator and $\Omega$ is a reflection in the inversion center located halfway along an $A \rightarrow B$ bond. The $\mathcal{T} \Omega$ symmetry implies that the magnon dispersion is even in $\mathbf{k}$.

The optical susceptibility tensor is calculated via the cross section for two-magnon excitations. In the linear spin wave approximation, the cross section is given by [30]

$$\chi^{(2)}_{\mathbf{q} \mathbf{q}^\prime} = \sum_{\mathbf{k} \mathbf{k}^\prime} \frac{q}{\mathbf{k}} \frac{q^\prime}{\mathbf{k}^\prime} \frac{\epsilon_{\mathbf{k}}}{\epsilon_{\mathbf{k}^\prime}} \frac{\epsilon_{\mathbf{k}^\prime}}{\epsilon_{\mathbf{k}}} \frac{\epsilon_{\mathbf{k}^\prime}}{\epsilon_{\mathbf{k}}} \frac{\epsilon_{\mathbf{k}}}{\epsilon_{\mathbf{k}^\prime}} \frac{\epsilon_{\mathbf{k}^\prime}}{\epsilon_{\mathbf{k}}},$$

(3)

Here $\epsilon_{\mathbf{k}} = (\epsilon_{ak} \beta_{-k})$, $R_{\mathbf{q} \mathbf{q}^\prime} = J(\epsilon a/\hbar)^2 \gamma q \gamma q^\prime$, and to simplify the notation we have defined $q \equiv |\mathbf{q}|$.

The matrix elements $\chi_{\mathbf{q} \mathbf{q}^\prime}$ give the form factor $M_{\mathbf{q} \mathbf{q}^\prime} = \sum |\chi_{\mathbf{q} \mathbf{q}^\prime}|^2$ of the Raman cross-section for two-magnon excitations. In the linear spin wave approximation, the cross section is given by $R_{\mathbf{q} \mathbf{q}^\prime} = \sum_{\mathbf{k} \mathbf{k}^\prime} \frac{q}{\mathbf{k}} \frac{q^\prime}{\mathbf{k}^\prime} \frac{\epsilon_{\mathbf{k}}}{\epsilon_{\mathbf{k}^\prime}} \frac{\epsilon_{\mathbf{k}^\prime}}{\epsilon_{\mathbf{k}}} \frac{\epsilon_{\mathbf{k}^\prime}}{\epsilon_{\mathbf{k}}} \frac{\epsilon_{\mathbf{k}}}{\epsilon_{\mathbf{k}^\prime}} \frac{\epsilon_{\mathbf{k}^\prime}}{\epsilon_{\mathbf{k}}}$ with $\Delta_q = \hbar \omega - \hbar \omega'$. The cross section is shown in Fig. 4(a) for a right-handed circularly polarized laser, scattered into either a left- or right-handed photon. At normal incidence, there is an almost complete polarization selection favoring scattering into left-handed photons. This is accompanied by an almost perfect selection rule favoring magnon excitation at the K point, as seen by the $\mathbf{k}$ dependence of the form factor $M_{\mathbf{k} \mathbf{k}_D}$ in Fig. 4(b). As the angle of incidence is decreased, the relative contributions for scattering into left- and right-handed photons approach each other and become identical for an in-plane laser. This can be understood by considering the projection of the electric field onto the substrate plane: At normal incidence, the projected field is circular and angular momentum conservation requires scattering into a mode of opposite handedness. For in-plane incidence, the projected field is linear and thus consists of equal parts left- and right-handed photons.

The optical susceptibility tensor is calculated via the second-order Kubo formalism [25,26] using the magnon current operator $J$ [32]. The magnons are assumed to be in initial
equilibrium at a temperature $T$ and the photons to be in the initial state $|n_{\text{in}}\rangle\prod_{\alpha} |0_{\alpha}\rangle$, with a single macroscopically populated photon mode corresponding to the incident laser. Since the experimental setup of Fig. 2 is insensitive to the energy and polarization of the scattered photons, the current is integrated over scattered photon states.

The magnon photocurrent consists of a Stokes and an anti-Stokes component [32], with the latter vanishing in the zero temperature limit. Further, both components have contributions from both the diagonal and off-diagonal terms of the magnon current operator. For the spin parameters considered here [36,37], the diagonal Stokes term is larger than the remaining contributions by about three orders of magnitude [see Fig. 3(d)], and the photo-induced magnon current is therefore given to a very good approximation by

$$
\langle J \rangle(q_{\text{in}}) = \frac{2G}{\hbar \omega_{q_{\text{in}}}} \int \frac{d\mathbf{k}}{(2\pi)^2} (n_{k\alpha} + n_{k\beta} + 1) 
$$

$$
\times (v_{\kappa\alpha} + v_{\kappa\beta}) |\langle n_{q_{\text{in}}} | \rangle|^2 \Delta_{\mathbf{k}}.
$$

Here $G$ is a constant depending on the intensity $I$ and photon energy $\hbar \omega_{q_{\text{in}}}$ of the incident laser, $n_{k\alpha}$ ($n_{k\beta}$) is the thermal magnon population, $\Gamma^{-1}$ is a phenomenological magnon lifetime, and $\Delta_{\mathbf{k}} = \hbar \omega_{q_{\text{in}}} - \epsilon_{\kappa\alpha} - \epsilon_{\kappa\beta}$. Taking $I = 10^{12}$ W/cm$^2$ and $\hbar \omega_{q_{\text{in}}} = 1$ eV, we find $G \approx 3.6 \times 10^{-12}$ meV/Å.

Since the magnon pairs $|\kappa\alpha, \beta\kappa\rangle$ carry zero net momentum, momentum conservation forces the wave vectors of the incident and scattered photons to be identical. Taking $q_{\text{in}} = q = g (\cos \phi \sin \theta, \sin \phi \sin \theta, -\cos \theta)$, where $\theta$ and $\phi$ are defined in Fig. 1, the polarization of the incident laser can be written as $\mathbf{e}_{\text{in}} = (\hat{e}_1 - i \zeta \hat{e}_2)/\sqrt{2}$. Here $\hat{e}_1$, $\hat{e}_2$, and $\mathbf{q}$ constitute a right-handed coordinate system and $\zeta = 1$ ($\zeta = -1$) for right-handed (left-handed) polarization. Evaluating the symmetry allowed elements of the susceptibility tensor from Eq. (4), only $\sigma = \sigma_{\text{yyyy}}$ is found to give a nonzero contribution to $\langle J \rangle$, see Eq. (1).

To understand the origin and angular dependence of the magnon photocurrent, we consider the momentum space structure of the excited magnon population for different $(\theta, \phi)$. At normal incidence ($\theta = 0$), the excited magnon population has $C_3$ rotational symmetry and, depending on the field chirality, magnons are excited mainly at $K$ or at $K'$ [see Fig. 4(d)]. Expanding the Raman form factor $M_k$ around $K_z = 4\pi \tau/(3\sqrt{3} \alpha \epsilon_z)$, with $\tau = \pm 1$ at $K'$ ($K$), we find $M_k = 3(RS\alpha)^2/2(1 - \eta \tau) + O(k^2)$. Thus, we find a near perfect optical selection rule for two-magnon excitations in honeycomb antiferromagnets. However, the $C_3$ symmetry leads to a vanishing current when integrated over the Brillouin zone. Analogously, at in-plane incidence ($\theta = \pi/2$), the excited magnon population is $C_2$ symmetric, again leading to a vanishing integrated current. In the intermediate range $0 < \theta < \pi/2$, the magnon population is asymmetric and interpolates between the limiting cases at $\theta = 0$ and $\theta = \pi/2$, leading to a maximal current at $\theta = \arctan \sqrt{2} \approx \pi/3$ (see Fig. 2).

The angular dependence of $\langle J \rangle$ is understood by noting that as a function of $\phi$, the maxima of the magnon population rotate around the $K$ or $K'$ points at a distance $d(\theta)$ with $d(0) = 0$ and $d(\pi/2) = a/2$. The period of the rotation results from the coincidence of the in-plane projected polarization at $\phi$ and $\phi + \pi$. This leads to a clockwise (anticlockwise) rotation of the current with a period $\pi$ for right-handed (left-handed) fields.

In conclusion, the current generation process creates magnon pairs $|\alpha\beta, \beta\kappa\rangle$ with zero net momentum and net angular momentum $2h$. This requires absorption and emission of photons with net angular momentum, and thus circularly polarized light. Since the process is symmetric under the transformation $\mathbf{k} \rightarrow -\mathbf{k}$, the magnon current and MCPGE requires an asymmetric excited magnon population that is achieved by irradiating the system at an oblique angle. Chiral magnon photocurrents thus arise from the interplay of momentum imbalance induced by the chiral optical field and the net angular momentum carried by magnon pairs.

To summarize, we have proposed an all-optical mechanism to generate magnon photo-currents via two-magnon Raman scattering. The current is directly proportional to the chirality of the incident laser and can therefore be controlled via the MCPGE. For realistic fields, the magnon current should be measurable with existing technology via the induced inverse spin Hall voltage in a Pt contact. Our results are independent of the details of the microscopic spin Hamiltonian and can be derived solely from the symmetries of the magnetic ground state and the requirement of angular momentum conservation, indicating that the MCPGE should be a generic feature of a large class of antiferromagnetic insulators.

The present symmetry analysis of honeycomb lattice antiferromagnets is straightforwardly extended to general magnetic point groups and, in general, we expect the MCPGE current to compete with currents insensitive to the polarization. However, for certain point groups, the optical susceptibility vanishes by symmetry, thus prohibiting the generation of magnon photocurrents. This is exemplified by the square lattice antiferromagnet, where an additional site inversion symmetry forces both the photocurrent and the magnon Berry curvature to vanish.

Our results suggest a deeper link between the magnon photocurrent found in this work and the Berry curvature, which should be explored in future works. We also note the close analogy of the optical selection rules discussed above to the selection rules for interband transitions in electronic
honeycomb systems [48]. The key role of quantum geometry for light-matter interaction has recently been noticed in the contexts of electronic flat-band systems [49] and nonlinear optical responses [50–52], and one can expect a similar role for the quantum geometry of magnon wave functions on the photon-magnon interaction. A natural extension of our work is to consider the photoinduced magnon current in topological magnetic systems where the integrated Berry curvature is nonzero [53] and where a quantized response could be present [54,55].

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