Tracing the phase transition of Al-bearing species from molecules to dust in AGB winds

Constraining the presence of gas-phase \((\text{Al}_2\text{O}_3)\)\(_n\) clusters

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Received date; accepted date

ABSTRACT

Context. The condensation of inorganic dust grains in the winds of evolved stars is poorly understood. As of today, it is not yet known which (clusters of) molecular gas-phase species form the first dust grains in oxygen-rich (C/O < 1) Asymptotic Giant Branch (AGB) winds. Aluminium oxides and iron-free silicates are often put forward as promising candidates for the first dust seeds.

Aims. We aim to constrain the dust formation histories in the winds of oxygen-rich AGB stars.

Methods. We have obtained ALMA observations with a spatial resolution of \(120 \times 150 \, \text{mas}\) tracing the dust formation region of a low mass-loss rate and a high mass-loss rate AGB star, respectively being R Dor and IK Tau. Emission line profiles of AlO, AlOH and AlCl are detected in the ALMA data and are used to derive a lower limit of atomic aluminium incorporated in molecules. This constrains the aluminium budget that can condense into grains.

Results. Radiative transfer models constrain the fractional abundances of AlO, AlOH, and AlCl in IK Tau and R Dor. We show that the gas-phase aluminium chemistry is completely different in both stars, with a remarkable difference in the AlO and AlOH abundance stratification. The amount of aluminium locked up in these 3 molecules is small, \(<1.1 \times 10^{-7}\), for both stars, i.e. only \(<2\%\) of the total aluminium budget. A fundamental result is that AlO and AlOH, being the direct precursors of alumina grains, are detected well beyond the onset of the dust condensation proving that the aluminium oxide condensation cycle is not fully efficient. The ALMA observations allow us to quantitatively assess the current generation of theoretical dynamical-chemical models for AGB winds. We discuss how the current proposed scenario of aluminium dust condensation for low mass-loss rate AGB stars at a distance of \(<1.5\, \text{R}_\odot\), in particular for the stars R Dor and W Hya, poses a challenge if one wishes to explain both the dust spectral features in the spectral energy distribution (SED), in interferometric data, and in polarized light signal. In particular, the estimated grain temperature of Al\(_2\)O\(_3\) is too high for the grains to retain their amorphous structure. We propose that large gas-phase \((\text{Al}_2\text{O}_3)\)\(_n\)-clusters \((n > 34)\) can be the potential agents of the broad 11 \(\mu\)m feature in the SED and in the interferometric data and we explain how these large clusters can be formed.

Conclusions. The ALMA data provide us with an excellent diagnostic tool to study the gaseous precursors of the first grains in AGB winds. The observations enable us to constrain theoretical wind models and to refine our knowledge of the chemical sequence followed by aluminium species when going through the phase transition from gaseous to solid-state species. Aluminium-bearing molecules only lock up \(<2\%\) of aluminium in the inner wind of IK Tau and R Dor. If the rest of aluminium would form solid-state dust species, there remain challenges to explain different sets of observational data. We hypothesize that large gas-phase \((\text{Al}_2\text{O}_3)\)\(_n\)-clusters \((n > 34)\) are the carrier of the broad 11 \(\mu\)m feature which is prominently visible in the SED of low mass-loss rate O-rich AGB stars.

Key words. Stars: AGB and post-AGB, Stars: mass loss, Stars: circumstellar matter, Stars: individual: IK Tau, R Dor and W Hya, instrumentation: interferometers, astrochemistry

1. Introduction

It is well known from observations that low and intermediate mass stars \((0.8\, \text{M}_\odot < \text{M} < 8\, \text{M}_\odot)\) develop a low-velocity \((v \sim \sim 5 – 15 \, \text{km/s})\) stellar wind at the end of their life during the Asymptotic Giant Branch (AGB) phase. At a mass-loss rate between \(10^{-8}\) to \(10^{-4}\, \text{M}_\odot/\text{yr}\), material is stripped away from the stellar surface. Convection-induced pulsations lift material to greater heights where the temperature is low enough for gas to
condense into dust grains. Radiation pressure on these grains is thought to be the main trigger for the onset of the stellar wind. While theoretical simulations based on this scenario predict stellar wind properties in broad agreement with observations of carbon-rich (C/O>1) AGB stars, more finetuning of the models is required for oxygen-rich (O-rich) AGB stars. Indeed, in these O-rich environments, the first dust seeds thought to form close to the stellar surface are metal oxides and pure Fe-free silicates such as Al$_2$O$_3$, SiO$_2$, Mg$_2$SiO$_3$, and MgSiO$_3$ (Woitke 2006). While their low near-infrared extinction efficiency prevents them from sublimating, it means that these glassy condensates make a negligible contribution to the radiative acceleration. The formation of both carbon and silicate grains (Höfner & Andersen 2007) or scattering of stellar radiation by micron-sized (∼0.3 µm) Fe-free silicates (Höfner 2008) have been proposed as possible alternatives to solve this acceleration deficit.

After its postulation in 2008 by Höfner et al., the latter scenario got more and more support from observations, the first ones reported by Norris et al. (2012) using VLT/NACO data of three low mass-loss rate AGB stars (R Dor, W Hya, and R Leo). The mid-infrared interferometric observations of the semi-regular AGB star RT Vir with the MIDI instrument at VLTI also lend support to the presence of iron-free silicates between 2 and 3 stellar radii (Sacuto et al. 2013). Recent polarized light data obtained with the VLT/SPIRE instrument offer us another way to look at the inner wind chemical and morphological structure. Again, these data prove the presence of grains close to the star albeit putting stringent constraints on the grain size is not obvious (Khouri et al. 2016; Ohnaka et al. 2016). However, neither the NACO or the SPIRE data can pinpoint the exact chemical constitution of these micron-sized transparent grains.

Considering the abundance of molecular species and the temperatures at which they can exist in solid phase, possible candidates for the first nucleation seeds are SiO, SiO$_2$, MgO, Fe, Al$_2$O$_3$, TiO and TiO$_2$ (Jeong et al. 2003). However, taking into account the thermodynamic properties, MgO nucleation is thought to be completely negligible in O-rich AGB stars. Although Al$_2$O$_3$ dust is stable at very high temperatures, gaseous Al$_2$O$_3$ has a low abundance, calling into question its role as the first candidate. For a long time, TiO and TiO$_2$ were considered to be the best candidates as primary condensates, since the nucleation rate of the more abundant SiO was thought to peak around 600 K (as based on the thermodynamic model of Schick 1960 using a single laboratory determination of the SiO vapour pressure), which is significantly lower than the typical temperatures at the inner edge of the dust shells. However, more recent laboratory experiments by Nuth & Ferguson (2006) and Gail et al. (2013) proved that the onset of SiO nucleation starts at much higher temperatures than was previously found, although the calculated SiO condensation temperatures are still ∼100 K lower than the observed ones (being around 880 K).

Another quest focuses on the potential chemical differentiation between grains formed in low mass-loss rate versus high mass-loss rate O-rich AGB stars. Observations indicate that low mass-loss rate stars form primarily dust that preserves the spectral properties of Al$_2$O$_3$, and stars with higher mass-loss rates form dust with properties of warm silicate oxides (Karovicova et al. 2013). It is absolutely unknown if the silicates form via a heteromolecular homogeneous nucleation process consuming Mg, SiO, and H$_2$O molecules (Goumans & Bromley 2012) or if the silicates form on top of the alumina grains (heterogeneous growth), hence gradually accelerating the wind. And be it now Fe-free silicates or aluminium-oxides that are the first solid-state species formed, another aspect that one might wonder about is how we could detect the (large) gas-phase clusters which are the intermediate steps between the simple molecules and micron-sized grains.

A promising way to unravel the intriguing coupling between nucleation and wind generation is by studying at high spatial resolution the molecules contributing to the dust formation. This possibility is offered by ALMA (the Atacama Large Millimeter/sub-millimeter array). We were granted ALMA Cycle 2 observing time (project 2013.1.00166.S) to investigate the molecular content in the inner wind region of the low mass-loss rate semi-regular AGB star R Dor (M$_\dot{\nu}$ ∼ 9 × 10$^{-8}$ M$_\odot$/yr) and the high mass-loss rate Mira star IK Tau (M$_\dot{\nu}$ ∼ 4.5 × 10$^{-6}$ M$_\odot$/yr). We obtained the first ALMA spectral scan for O-rich AGB stars in band 7 at a spatial resolution of ∼0.12′×0.05′. The full data scan will be presented in Decin et al. (2017). In this paper, we aspire to elucidate the role of aluminium-bearing molecules, clusters, and grains, in the stellar winds. The ALMA observations are presented in Sect. 2.4. Since the aim is to correlate the gaseous aluminium content with the amount of aluminium locked up into grains, we briefly summarize the most important dust properties of the targets in Sect. 2.3. Important additional information on the dust formation history in O-rich AGB stars also stems from another low mass-loss rate O-rich AGB star, W Hya. Where needed, we bring in additional constraints as derived from that target. Some properties of the three targets are introduced in Sect. 2.4. The results of the data analysis are presented in Sect. 3 and are discussed in the context of molecule, cluster, and dust formation in Sect. 4. The conclusions are summarized in Sect. 5.
lar radii (R*), after which the grains where coated with silicates around ~10 stellar radii) might take place.

R Dor is the closest AGB star to our Sun, with a gas mass-loss rate value of ~0.9–2 × 10^{-7} M_⊙/yr and an expansion velocity of only ~5.7 km/s (Schöier et al. 2004; Khouri 2014; Maercker et al. 2016; Van de Sande et al. 2017). It is a semi-regular variable with two pulsation modes having periods of 332 days and about 175 days, the latter one with much smaller amplitude (Bedding et al. 1998). Its angular diameter is ~60 mas (Bedding et al. 1997; Norris et al. 2012). From an analysis of Herschel and sub-millimeter data, Khouri (2014) and Van de Sande et al. (2017) derived that some 90% of atomic silicon is locked up in gaseous SiO, the remainder in silicates. VLT/NACO and SPHERE/ZIMPOL data support the presence of a close halo of large transparent grains (~0.3 μm) at ~1.5–2 R* (Norris et al. 2012; Khouri et al. 2016).

IK Tau is a high mass-loss rate Mira-type AGB star with a gas mass-loss rate of ~4.5 × 10^{-8} M_⊙/yr, an expansion velocity of 17.7 km/s (Decin et al. 2010a; Maercker et al. 2016), and a pulsation period of ~470 days (Wing & Lockwood 1973). The angular diameter is estimated around 60 mas (Decin et al. 2010a). Currently, a different number of molecules and some of their isotopologues have been discovered in IK Tau, including CO, HCN, SiO, SiS, SO, SO\(_2\), NaCl, NS, NO, HCO\(^+\), H\(_2\)CO, PO, PN, H\(_2\)S (Milam et al. 2007; Kim et al. 2010; Decin et al. 2010b). Be Beck et al. 2013, 2015; Velilla Prieto et al. 2016). Some molecules including SiO and SiS are depleted in the circumstellar envelope, possibly due to condensation onto dust grains. Other molecules such as HCN demonstrate the impact of pulsation-driven shocks in the inner wind zone which forces the chemistry into a non-equilibrium state.

W Hya resembles in many aspects the low mass-loss rate AGB star R Dor. Thanks to its proximity (~78 pc, Knapp et al. 2003) and its brightness it is also well studied with various observational techniques from the visible to the radio. This semi-regular variable has a light curve showing a clear periodicity with period of 389 days (Uttenthaler et al. 2011). The molecular abundance stratification in its circumstellar envelope was studied in detail by Khouri et al. (2014b). Based on an extensive grid of CO, SiO, H\(_2\)O and HCN lines (and some of their isotopologues) the thermodynamic structure of the wind was derived and they deduced that about one-third of the silicon atoms is locked up in dust particles. The SED of W Hya is characterized by the same dust emission peaks as R Dor (see Sect. 2.3) and also for this star large scattering grains in a halo close to the star are detected via polarized light signal (Norris et al. 2012; Ohnaka et al. 2016). W Hya was also observed by ALMA in band 7 (project 2015.1.01466.S, P.I. A. Takigawa) with a spatial resolution of ~0.4 mas at 3 selected frequency bands (330–331.3 GHz, 342.40–343.34 GHz, 344.03–345.91 GHz) encompassing the AIO N=9–8 and AIOH J=11–10 transition. AIO is detected in their data (Takigawa et al. 2016).

### 2.2.1. ALMA observing strategy

Spectral scans of IK Tau and R Dor were obtained covering the frequencies between 335–362 GHz, using four separate observations each, during August-September 2015. The observations and data reduction used the ALMA pipeline for calibration, followed by identifying and imaging the line-free continuum, which was then used for self-calibration. The solutions were applied to all data and spectral cubes were made adjusted to constant \(v_{\text{LSR}}\). The process is described in more detail in Decin et al. (2017); here, we concentrate on the parameters affecting the Al compound cubes. The astrometric accuracy is ~17 mas and the flux scale is accurate to ~7%. The relative accuracy (e.g., aligning different lines in the same source) is limited only by the signal-to-noise, S/N, and would be <1 mas for S/N of 200, or 33 mas (about 1 pixel) for a faint 3σ detection of a compact source. The rms noise (\(\sigma_{\text{rms}}\)) varies across the band depending on intrinsic atmospheric transmission and the weather at the time of observations. The final image parameters are summarised in Table 1. Owing to the different elevations as seen from ALMA, we achieved a higher resolution and used a smaller pixel size (30 mas versus 40 mas) for R Dor versus IK Tau. For each line, we made cubes at higher and lower spectral resolution (~80 mas at 3 selected frequency bands) encompassing the line-free bandwidth (spread between 335–362 GHz) for the continuum.

### 2.2.2. Al-bearing species detected with ALMA

Chemical models show that the most likely carriers of aluminium in the wind of oxygen-rich evolved stars are Al, AlH, AlO, AlOH, AlO\(_2\), AlCI, AlS, and AlO\(_2\) (see Fig. 16 in Sect. 4.1) a result by Gobrecht et al. (2016). The main isomers of AlO\(_2\) and Al\(_2\)O are linear and their rotational lines are not observable; nor is the homonuclear Al\(_2\) easily observable (Cai et al. 1991; Koput & Gertych 2004; Kamiński et al. 2016). AlOH does not have a rotational line transition in the targeted ALMA frequency range. The other three aluminium-bearing molecules are detected in IK Tau and R Dor with ALMA: AIO N=9–8 (rest frequency, \(\nu_{\text{rest}}\), at 345.457 GHz, lower state energy \(E_{\text{low}}=66\) K), AIOH J=11–10 (\(\nu_{\text{rest}}=346.156\) GHz, \(E_{\text{low}}=83\) K), and AlCI J=24–23 (\(\nu_{\text{rest}}=349.444\) GHz, \(E_{\text{low}}=193\) K).

| Species  | \(\text{Chan}^a\) | \(\text{Vel}^b\) | Beam | \(\sigma_{\text{rms}}\) |
|---------|-----------------|---------------|------|-------------------|
|         | (MHz)           | (km s\(^{-1}\)) | (mas x mas, P.A.) | (mJy) |
| **IK Tau** |                 |               |                  |       |
| Continuum | 15.2 × 10\(^3\) | 180×160, 27° | 0.047 |
| AICI     | 1.95            | 1.7           | 160×130, 43°     | 1.6   |
| AICI     | 5.9             | 5             | 200×160, 42°     | 1.4   |
| AIIOH    | 1.95            | 1.7           | 150×140, 22°     | 5.0   |
| AIIOH    | 5.9             | 5             | 190×170, 1°      | 2.4   |
| AIO      | 1.95            | 1.7           | 160×130, 15°     | 5.0   |
| AIO      | 5.9             | 5             | 190×170, 20°     | 2.6   |
| **R Dor** |                 |               |                  |       |
| Continuum | 11.6 × 10\(^3\) | 150×140, 5°   | 0.047 |
| AICI     | 0.97            | 0.9           | 150×130, 20°     | 2.7   |
| AICI     | 2.5             | 2.2           | 180×180, 10°     | 1.4   |
| AIIOH    | 0.97            | 0.9           | 170×120, 48°     | 3.8   |
| AIIOH    | 2.5             | 2.2           | 200×160, 48°     | 2.4   |
| AIO      | 0.97            | 0.9           | 160×130, 26°     | 4.0   |
| AIO      | 2.5             | 2.2           | 190×160, 30°     | 1.8   |

Notes. (a) ‘Chan’ is the channel width for the line cubes, or the total line-free bandwidth (spread between 335–362 GHz) for the continuum. (b) ‘Vel’ is the spectral resolution of the image cube. (c) P.A. is the position angle measured from North to East.
The transitions of these three molecules are split up by hyperfine components due to the nuclear spin, $I = \frac{5}{2}$, of aluminium. AlOH and AlCl are closed-shell species with a $^1\Sigma^+$ ground state. AlO is a radical with a $^2\Sigma$ ground state. The rotational levels of this molecule are therefore split by both fine and hyperfine interactions. The net result is that each rotational transition consists of $10 − 12$ favourable, closely spaced, hyperfine components (Tenenbaum & Ziurys 2009, 2010).

Figure 1 shows the flux densities extracted for an aperture size of 320 mas (300 mas) and 800 mas (1000 mas) for IK Tau (R Dor). The channel maps for the individual transitions are shown in Fig. 2–5 for IK Tau and in Fig. 6–10 for R Dor. Table 2 gives the measured properties of each molecular transition, including the velocity width, the shift of the centroid w.r.t. the LSR velocity of the star, the angular width, and the peak flux and integrated flux within the specified velocity interval. The angular width has been obtained from the zeroth moment (total intensity) by measuring the mean flux in annuli of 60 (80) mas, centred on the position of R Dor (IK Tau), assumed to be the continuum peak. The angular size was taken as the distance out to $2 \sigma_{\text{rms}}$. The measurements were also used to compute the azimuthally averaged flux densities, in order to compare with 1D models solving the non-LTE radiative transfer equation for the specific molecule (Sect. 3) and with models solving the chemical network (so-called ‘forward’ chemistry models) by Gobrecht et al. (2016) in Sect. 4. The emission of some molecular transitions shows some irregular morphologies (as described in the next subsections) but there is no obvious preferred direction, so this is a reasonable approximation although not allowing for clumpiness.

2.2.3. IK Tau

AlO: Looking at Fig. 2, AlO remains at first sight barely detected in IK Tau. This is reflected by the line profile for the 320 mas extraction aperture (Fig. 1). However, enlarging the extraction aperture to 800 mas, a clear signature of AlO emission is seen with a peak flux of 0.19 Jy and integrated line flux of 3.2 Jy km s$^{-1}$. The SMA observations by De Beck et al. (2017) also show a weak AlO emission feature with an integrated line flux of 2.33 Jy km s$^{-1}$ for an aperture of $1 \times 1''$. This points toward faint extended AlO emission that is probably genuinely clumpy. To verify this idea, we have averaged the AlO emission over 5 channels and smoothed the emission with a 0$''$.5 Gaussian kernel; see Fig. 3. Albeit the signal-to-noise ratio is still low and we caution that the smoothing is on a scale comparable to the maximum recoverable scale (MRS), this figure indeed hints at extended clumpy emission.

AlOH: The channel maps of IK Tau show a clear detection of AlOH with a peak strength around 0.07 − 0.12 Jy (depending on the extraction aperture; Fig. 4). The emission is centred around the peak of the continuum emission and has an angular width of $\sim$240 mas.

AlCl: Around the $\nu_{\text{LSR}}$ of $\sim$35 km/s almost no AlCl emission is seen, but the emission increases in strength at blue-shifted velocities (Fig. 5). This is reflected in the asymmetric AlCl line profile in Fig. 1.

2.2.4. R Dor

AlO: The bright AlO N=9-8 is easily picked up by the ALMA instrument, with a peak flux of $\sim$0.13 − 0.17 Jy for the two dif-
Table 2. Spectral properties of AlO, AlOH, and AlCl as observed with ALMA in IK Tau (upper part of the table) and R Dor (lower part). Values for the velocity width, velocity asymmetry, angular width, and peak and integrated flux are only given in the case of a clear detection.

| Molecule   | Aperture 320 mas | Aperture 800 mas | Aperture 300 mas | Aperture 1000 mas |
|------------|------------------|------------------|------------------|------------------|
| AlO N=9−8  | 3.40             | −0.32            | 0.036            | 0.247            |
| AlOH J=11−10 | 11.84           | 1.06             | 0.073            | 0.466            |
| AlCl J=24−23| 6.70             | −2.92            | 0.024            | 0.228            |
| IK Tau     | 32.30            | 14.98            | 0.186            | 3.211            |
|            | 800              | 640              | 160              |                  |
| R Dor      | 51.00\(^{b}\)   | 3.67             | 0.128            | 4.032            |
| AlOH J=11−10 | 3.38            | −0.36            | 0.027            | 0.119            |
| AlCl J=24−23| 3.35             | 2.65             | 0.021            | 0.113            |

Notes.\(^{(a)}\) The shift of the centroid w.r.t. the LSR velocity of the star is obtained by dividing the value of the ‘velocity asymmetry’ by two. \(^{(b)}\) Large velocity width is caused by the hyperfine structure; see Sect. 3.

Fig. 2. Channel maps (colour scale in mJy) of the AlO N=9−8 transition in IK Tau. White contours are the continuum at (−1, 1, 4, 16, 64, 256)×0.3 mJy. The ordinate and co-ordinate axis give the offset of the right ascension and declination, respectively, in units of arcseconds. The ALMA beam size is shown in the bottom left corner of the upper panel.

Different extraction apertures. The emission is smooth and concentrated around the peak of the continuum emission (Fig. 6). At an offset of ∼280 mas to the south-east, enhanced AlO emission is seen in many channel maps (Fig. 7). At the same offset location other molecules (including AlOH, SO, SiO, CO, and SO\(_2\)) show excess emission as well with the main peak having a blue-shifted frequency offset of 15−20 MHz.

AlOH: The AlOH emission in R Dor is very weak and just above 3 \(\sigma_{\text{rms}}\) for the 300 mas extraction aperture (Fig. 1).
Fig. 3. Same as for Fig. 2 but the AlO emission is averaged over 5 channels and smoothed with 0′′5 Gaussian kernel.

Fig. 4. Same as for Fig. 2 but for AlOH J=11−10.
The main emission around $v_{\text{LSR}}$ is slightly off-center (as compared to the peak of the continuum emission; Fig. 8). As noted already for AIO, a brighter clump of emission is visible around 280 mas to the south-east (Fig. 9).

**AlCl:** Almost no AlCl emission is visible around $v_{\text{LSR}}$ for the 300 mas aperture (Fig. 10), but brighter emission becomes apparent at larger velocities with a peak flux around 0.02–0.06 Jy and an integrated flux of 0.1–0.3 Jy km s$^{-1}$ (depending on the extraction aperture).

The different velocity offsets for AlCl (on the red-shifted versus blue-shifted sides of the systemic velocity) for R Dor versus IK Tau cautions us to consider a potential blend or misidentification of this species.

### 2.3. Infrared continuum emission

R Dor, IK Tau, and W Hya have been studied using different spectroscopic, interferometric, polarimetric, and imaging instruments. With the aim to discuss the aluminium fraction locked up into grains, we shortly summarize in this section the results published in the literature that are relevant for this study.

Both R Dor and W Hya have been observed with the Short Wavelength Spectrometer (SWS) on board of the Infrared Space Observatory (ISO) using the AOT01 observing mode. R Dor was observed at so-called speed 1, while for W Hya both speed 1 and speed 3 were used. The spectral resolution for the speed 3 data is around 700–1000, and is a factor of ~2 worse for the speed 1 data. Interferences in the instrument cause however fringes in the ISO band 3 data (12-29 μm), particularly in the case of the higher resolution observations. Unfortunately, no ISO-SWS data are available for IK Tau, the only infrared spectrum available being IRAS-LRS data (see Fig. 11).

SPHERE/ZIMPOL data were recently obtained for R Dor and W Hya (Khoury et al. 2016, Ohnaka et al. 2016) confirming the earlier result by Norris et al. (2012) that a halo of large transparent grains is present at ~1.5–3 $R_\star$. Estimated grain sizes are around 0.3-0.5 μm and Fe-free silicates or Al$_2$O$_3$ are put forward as the possible dust species that produce the scattered light.

Zhao-Geisler et al. (2011) monitored W Hya with MIDI/VLTI (8–13 μm, spectral resolution of 30) during nearly three pulsation cycles. From the spectrally dispersed visibility data, the authors concluded that the Fe-rich silicate emission seen around 10 μm in the ISO-SWS data arises from a region fairly far away from the star, at radii larger than 30 times the photospheric radius. Using image reconstruction techniques, Zhao-Geisler et al. (2015) were able to spatially resolve the dust formation region close to the star and deduced that the data signal the presence of a dust layer of presumably amorphous aluminium oxide (Al$_2$O$_3$) at ~2 $R_\star$. The observations suggest that the formation of amorphous Al$_2$O$_3$ occurs mainly around or after visual minimum (Zhao-Geisler et al. 2012).

VLTI/MIDI data are also available for R Dor. However the fringe-track data do not contain any interferometric signal. Probably the beams were not overlapped correctly, as the data were taken for test purposes. No MIDI data are available for IK Tau.

To derive the dust chemical composition and shed light on the mass-loss mechanism, the SED of W Hya together with infrared images and optical scattered light fractions were analysed by Khouri et al. (2015). The only way to explain all observed signatures, and in particular the amorphous Al$_2$O$_3$ emission in the...
SED, was by implementing in their radiative transfer model a so-called gravitationally bound dust shell (GBDS) close to the star at around 1.5 to 3 stellar radii. This GBDS is a shell of dust particles for which the ratio of the radiation pressure on the grains to the gravitational attraction (often called the $\Gamma$-factor) is still smaller than 1 so that the dust particles can reside close to the star without being pushed outward. This allows the material to potentially grow in size, and only once their size is larger than 0.1-0.3 $\mu$m, $\Gamma$ can become larger than 1. This idea of a GBDS was recently shown to fit well with the theoretical dynamical wind models of Höfner et al. (2016), who allowed for the formation of composite grains with an Al$_2$O$_3$ core and a silicate mantle at slightly larger distances than the Al$_2$O$_3$ GBDS shell so to give the wind a kick start. The location of the GBDS coincides with the region where large transparent grains are detected in polarized light images (Norris et al. 2012; Ohnaka et al. 2016), albeit this does not imply by necessity that the species responsible for the Al$_2$O$_3$ emission in the SED are the same ones that cause the stellar light to be scattered. Thus, it is still possible that the scattering agents are Fe-free silicates, since these can remain fairly cold, and so not produce signature in the thermal infrared.

The poor quality of the infrared continuum data of IK Tau led us to decide not to analyse the dust content in this object, but to focus on the dust composition of R Dor and W Hya. We combined the available IR data for the latter two objects and subtracted the stellar continuum (represented as a blackbody with temperature of 3000 K for R Dor and of 2500 K for W Hya) in order to visualise better their dust spectral features; see Fig. 13. The emission bands of some dust aluminium bearing dust species are plotted, as well as some CO$_2$ and H$_2$O molecular emission features.

![Fig. 6. Channel maps (colour scale in mJy) of the AlO N=9-8 transition in R Dor. White contours are the continuum at ($−1$, 1, 4, 16, 64, 256)×0.15 mJy. The ordinate and co-ordinate axis give the offset of the right ascension and declination, respectively, in units of arcseconds. The ALMA beam size is shown in the bottom left corner of the upper panel.](image)
3. Results: Abundances of aluminium-bearing molecules

To establish the abundance and distribution of AlO, AlOH, and AlCl, we have modelled the ALMA data using a non-LTE radiative transfer model of the circumstellar envelope (CSE). We use a code based on the ‘Accelerated Lambda Iteration’ (ALI) method (Maercker et al. 2008), which allows us to retrieve the global mean molecular density by assuming a 1D geometry. Collisional excitation rates have not been published for any of these three molecules. For that reason, we have used the values for the HCN-H$_2$ system (Green & Thaddeus 1974) as substitute for AlOH (cf. Tenenbaum & Ziurys 2010), and of SiO-H$_2$ (Dayou & Balança 2006) for AlO and AlCl (cf. Kamiński et al. 2016), scaling for the difference in molecular weight. The collisional rates are used in the form they appear in the LAMDA

Fig. 7. Same as for Fig. 6 but zooming into the AlO emission in the inner 0.2 region.
Fig. 8. Same as for Fig. 6 but for AlOH J=11−10.

database[^1] (Schöier et al. 2005). To check for the dependency on collisional excitation rates, we also ran models using the CS-H$_2$ cross sections (Turner et al. 1992) and found no significant difference in results. The first 30 rotational levels in the ground vibrational state were considered for AlOH and the first 40 ones for AlO and AlCl. Our treatment of the radiative transfer does not deal with the (hyper)fine structure components, and is therefore limited to the prediction of rotational lines $N \rightarrow N'$ or $J \rightarrow J'$ with $\Delta N$ or $\Delta J$ equal to 1. Therefore, all levels treated are described by one quantum number, $N$ or $J$. The final line profile is computed by splitting the predicted total intensity over the different (hyper)fine components according to their relative quantum-mechanical line strength, $S$, as given in CDMS[^2] (Müller et al. 2001, 2005). This approach is only valid under LTE conditions.

For an angular diameter of 20 mas and a distance of 260 pc, the stellar radius of IK Tau is $\sim 3.8 \times 10^{13}$ cm, while the angular diameter of 57 mas and the distance of 60 pc translates into a stellar radius of $\sim 2.5 \times 10^{13}$ cm for R Dor. The gas kinetic temperature is assumed to follow a power law

$$T_{\text{gas}} = T_\star \left( \frac{R_\star}{r} \right)^{-\epsilon},$$

and the gas velocity profile is parametrized using a $\beta$-type law

$$v_{\text{gas}} = v_0 + (v_\infty - v_0) \left( 1 - \frac{r_0}{r} \right)^\beta,$$

with $r$ the distance to the star, $v_\infty$ the terminal velocity, and $v_0$ the velocity at radius $r_0$ at which the wind is launched and which is set to the local sound speed. The gas velocity within the dust condensation radius, $r < r_0$, is assumed to be 2 km/s. The turbulent velocity for both stars is assumed to be 1 km/s. The gas density, $\rho(r)$, is calculated from the equation of mass conservation

$$\dot{M} = 4\pi r^2 v(r) \rho(r).$$

The main input parameters for R Dor and IK Tau are listed in Table 3 following Maercker et al. (2016). These properties are simplified estimates, for example the velocity structure inside the dust formation radius is complex, but are adequate for 1D modelling in the regions where these Al compounds have been observed. For all molecular species, the fractional abundance structure with respect to H$_2$ was varied until a fit with the ALMA azimuthally averaged flux density was achieved (see Fig. 11). In some cases, the fractional abundance declines according to a Gaussian profile centred on the star, and hence is described by following equation

$$f(r) = f_0 \exp \left( -\left( \frac{r}{r_e} \right)^2 \right),$$

with $f_0$ the initial abundance and $r_e$ the $e$-folding radius.

The retrieved fractional abundance structures are shown in Fig. 14 the fit to the ALMA data in Fig. 11 Clearly both stars show a very different Al-chemistry. For IK Tau, AlOH could be modelled assuming a Gaussian distribution with a peak central abundance of $4.4 \times 10^{-9}$ and an $e$-folding radius, $r_e$, of 22 R$_\star$. As could be deduced already from Fig. 1 and Fig. 3, the AlO emission might be clumpy not showing a centrally peaked abundance structure. The data could be modelled assuming a constant
Table 3. Input parameters for the non-LTE radiative transfer modeling

|                | R Dor     | IK Tau    |
|----------------|-----------|-----------|
| $T_\star$ [K]  | 2400      | 2100      |
| $\epsilon$    | 0.65      | 0.6       |
| $v_\infty$ [km/s] | 5.7    | 17.5      |
| $\beta$        | 1.5       | 1.2       |
| $r_0$ [cm]     | $5.3 \times 10^{13}$ | $2.38 \times 10^{14}$ |
| $M$ [M$_\odot$/yr] | $1.6 \times 10^{-7}$ | $5 \times 10^{-6}$ |
| $L$ [L$_\odot$] | 6500      | 7700      |

abundance of $4.4 \times 10^{-8}$ from 50–160 R$_\star$. If the AlCl identification is correct (see Sect. 2.2), then the data are compatible with a Gaussian distribution with peak central abundance of $8.4 \times 10^{-8}$ and $2.5 \times 10^{-8}$ and $\epsilon$-folding radius of $3.8$ R$_\star$ and $2.4$ R$_\star$, respectively. The good correspondence between the observed and predicted emission of AlO in R Dor is shown in Fig. 15.

While we can trace the fractional abundance above $1 \times 10^{-9}$ within $\sim 150$ R$_\star$ for IK Tau, the ALMA Al-data of R Dor only cover the first 25 R$_\star$. The factor $\sim$6 difference in spatial extent is in line with the factor $\sim$50 in mass-loss rate (and hence sensitivity to some particle density assuming a density law which is proportional to $r^{-2}$).

Assuming a solar aluminium content of Al/H = $3 \times 10^{-6}$, our results imply that for both stars only a small fraction of aluminium ($\lesssim 2\%$) is locked up in AlO, AlOH, and AlCl.
4. Discussion

The analysis of the ALMA data leads to a direct determination of the mean fractional abundances of AlO, AlOH, and AlCl in the inner winds of R Dor and IK Tau. These results can be compared quantitatively to the theoretical model predictions solving the chemical network for IK Tau by Gobrecht et al. (2016), and hence bring about the first qualitative assessment of this kind of dynamical-chemical models (Sect. 4.1). The amount of aluminium locked up in gaseous species turns out to be low, leaving ample of room for aluminium to be incorporated into dust grains. However, as we will discuss in Sect. 4.2, the estimated grain temperatures for aluminium oxide (Al$_2$O$_3$) at ~2 R$_*$ is high suggesting that the grains are annealed and hence have a crystalline lattice structure. This outcome implies a tension in the interpretation of the 11 µm spectral feature, present in the SED and interferometric data. We hypothesize that large gas-phase aluminium oxide clusters are the cause of the 11 µm feature, and explain how these large clusters can be formed (Sect. 4.3).

4.1. The gas-phase aluminium budget

The deduced AlO, AlOH, and AlCl abundances of IK Tau can be compared directly to the chemical predictions by Gobrecht et al. (2016). They modelled the synthesis of molecules and dust in the inner wind of IK Tau ($r < 5$ R$_*$) by considering the effect of periodic shocks induced by the stellar pulsation. The non-equilibrium chemistry in the shocked gas-layers was followed between 1 R$_*$ and 10 R$_*$ by solving a chemical kinetic network including 100 species and 424 reactions. The condensation of dust is described by a Brownian formalism using the simplifying assumption that the gaseous dimers of forsterite (Mg$_2$SiO$_4$), enstatite (MgSiO$_3$) and alumina (Al$_2$O$_3$) are the initial dust seeds and considering coalescence and coagulation of these dimers to form the dust grains.

The aluminium species in the network of Gobrecht et al. (2016) include Al, AlH, AlO, AlOH, AlO$_2$, AlCl, Al$_2$, and Al$_2$O$_3$. The aluminium dust precursors are described by Al$_2$O$_2$, Al$_2$O$_3$, and Al$_2$O$_6$. The predicted abundances of the aluminium species as function of radius and phase are shown in Fig. 16 and 

4 The pulsation phase is defined as the decimal part of $(t - T_0)/P$, with $T_0$ the epoch of the start of the pulsation cycle and $P$ the period.
sumoto et al. (2008), the ALMA data of IK Tau are obtained around $\phi = 0.98$. The methodology applied by Gobrecht et al. (2016) implies that a relative comparison between the retrieved and predicted molecular abundance stratifications is best to be done using the first panel of Fig. 16 while the absolute scaling can be seen in Fig. 17. Taking the predicted abundances at $5 \, R_*$, (bottom panel in Fig. 17) at phase $\phi = 0.98$ as representative values for the comparison with the profiles retrieved from the ALMA data (left panel in Fig. 14), we can see that both the observations and chemical models predict a higher abundance for AlO than for AlO. However, the retrieved AlOH abundance at $5 \, R_*$ is 2 orders of magnitude lower than predicted. The ALMA data indeed show that the fractional AlO abundance ($r < 50 \, R_*$) is very low ($< 10^{-10}$) in accord with the predictions, but remarkably we see that an active Al-chemistry is taking place further out in the wind yielding an increase in AlO emission. We derive for IK Tau a mean AlO fractional abundance of $\sim 5 \times 10^{-8}$ between 50–150 $R_*$, with the emission mainly arising from clumps at that radial distance. The increase in AlO abundance coincides with a strong decrease in AlOH abundance suggesting that AlOH is converted to AlO. Another possibility is that desorption or sputtering release AlO from grains back into its gaseous form. If no line-blend is blurring the AlCl identification, then the ALMA data show that the AlCl abundance in IK Tau is a factor $\sim 40$ higher than predicted.

![Fig. 11. Azimuthally averaged flux density in function of the angular distance from the central star for IK Tau (top) and R Dor (bottom), respectively. The ALMA data are shown in red, with the vertical bars denoting the uncertainty. The radiative transfer model predictions are displayed in blue (see Sect. 3).](image)

![Fig. 12. Infrared spectrum of R Dor (black, full line), W Hya (grey, full line, scaled with a factor 1.5) and IK Tau (red, dashed line). Spectral features arising from dust species such as crystalline and amorphous Al$_2$O$_3$, gehlenite (Ca$_2$Al$_2$SiO$_7$), and so-called astronomical silicates (amorphous olivines with different relative magnesium and iron fractions; de Vries et al. 2010) are indicated.](image)

For a period of 470 days and with $T_0$ at JD$\sim$2453025 (Matsumoto et al. 2008), the ALMA data of IK Tau are obtained around $\phi = 0.98$. The methodology applied by Gobrecht et al. (2016) implies that a relative comparison between the retrieved and predicted molecular abundance stratifications is best to be done using the first panel of Fig. 16 while the absolute scaling can be seen in Fig. 17. Taking the predicted abundances at $5 \, R_*$, (bottom panel in Fig. 17) at phase $\phi = 0.98$ as representative values for the comparison with the profiles retrieved from the ALMA data (left panel in Fig. 14), we can see that both the observations and chemical models predict a higher abundance for AlO than for AlO. However, the retrieved AlOH abundance at $5 \, R_*$ is 2 orders of magnitude lower than predicted. The ALMA data indeed show that the fractional AlO abundance ($r < 50 \, R_*$) is very low ($< 10^{-10}$) in accord with the predictions, but remarkably we see that an active Al-chemistry is taking place further out in the wind yielding an increase in AlO emission. We derive for IK Tau a mean AlO fractional abundance of $\sim 5 \times 10^{-8}$ between 50–150 $R_*$, with the emission mainly arising from clumps at that radial distance. The increase in AlO abundance coincides with a strong decrease in AlOH abundance suggesting that AlOH is converted to AlO. Another possibility is that desorption or sputtering release AlO from grains back into its gaseous form. If no line-blend is blurring the AlCl identification, then the ALMA data show that the AlCl abundance in IK Tau is a factor $\sim 40$ higher than predicted.

The stellar angular diameter of IK Tau is $\theta_D \sim 20 \, \text{mas}$ (Decin et al. 2010). The inner radius of dust detected by Dehaes et al. (2007) and inferred by Richards et al. (2012) is at 6–10 $R_*$, but these observations were not sensitive to the potential presence of transparent grains closer to the star. The ALMA beam of $\sim 0''12 \times 0''15$ is hence too large to confirm the predicted strong radial variation in molecular abundance within 5 $R_*$ (as visible in Fig. 16). The angular diameter of R Dor is much larger, $\theta_D \sim 57 \, \text{mas}$ (Bedding et al. 1997; Norris et al. 2012; Khouri et al. 2016). Although a direct comparison with Fig. 16–17 should be done with care — since the shock velocities are expected to be smaller for R Dor — our ALMA data do not cor-
Fig. 13. Continuum subtracted and normalized SED of R Dor and W Hya (in full black and gray lines, respectively). Characteristic (scaled) emission patterns of different dust species are shown in the coloured dashed lines. The gray vertical dotted lines indicate CO$_2$ molecular emission (Justtanont et al. 1998; Ryde et al. 1999).

Fig. 14. Retrieved fractional abundance structure [AlO/H$_2$], [AlOH/H$_2$], and [AlCl/H$_2$] for IK Tau (left) and R Dor (right).

robate any strong radial variation in AlO and AlOH abundance within the first 10 stellar radii. In addition, the AlCl abundance decreases with radial distance in contrast to the chemical network predictions.

The resolution of our ALMA observations does allow us to trace the molecular abundances at the smallest radii at which dust has been detected (being around 6—10 $R_*$ for IK Tau and around 2 $R_*$ for R Dor). AlO and AlOH are directly associated with the nucleation of alumina and their retrieved abundances are indeed much lower than in the pure gas-phase models of Gobrecht et al. (2016). But clearly, not all available AlO and AlOH molecules participate in that dust formation process. In addition, the ALMA results on R Dor prove that a second phase of dust formation, proposed to occur slightly beyond the GBDS, is (almost) not consuming AlO. This supports the scenario suggested by Höfner et al. (2016) that the growth of silicates (potentially on top of already existing alumina grains) is a trigger for the wind to get launched.

It would be of interest to monitor the changes in abundance structure in function of the pulsation phase and confront them with the predictions shown in Fig. 17. This kind of data could then be used to benchmark and improve current forward chemistry models that implement gas dynamics. We note that Kamiński et al. (2016) have reported some variability in the AlO
Fig. 15. Comparison between the extracted ALMA AlO spectra of R Dor (green) and the predicted line profile (red) for an AlO abundance structure as given in Fig. 14 for the 300 mas (left) and 1000 mas (right) extraction aperture.

Fig. 16. Predicted abundances of aluminium-bearing molecules with respect to the total gas number density as a function of radius. Chemical models are based on the pulsation-induced shock dynamics presented by Gobrecht et al. (2016). Model simulations for a star resembling IK Tau at phase $\phi = 0.0$ (top) and $\phi = 0.5$ (bottom).

Although the current comparison points toward improvements to be made in the chemical model predictions, a conclusion from the ALMA data in combination with these models is that the fraction of aluminium that is locked up in simple aluminium-bearing molecules seems small. I.e., the combined fractional abundance of Al-molecules which are thought to form easily in the inner wind region is only $\sim 5 \times 10^{-8}$. Even more, since the formation of the more complex Al$_2$O$_3$ and its dimer ($\text{Al}_2\text{O}_3$)$_2$ is described by termolecular recombination and hence requires high densities, these higher order molecules will also only consume a tiny fraction of the available aluminium (see Fig. 17) where one can see that the alumina dimers only form at 1 R$_*$ and at late phases; i.e. these larger molecules too can be neglected as major sink of aluminium.

The most difficult gaseous aluminium form to constrain is that of atomic aluminium. The atomic aluminium abundance is predicted to be high when the parcel of material is close to the star ($r < 2.5$ R$_*$) for phases $\phi > 0.2$ (see Fig. 17). Exactly at the shock front, phase $\phi = 0$, the high temperature ensures a high Al abundance, but as a consequence of the declining temperature for later phases the atomic Al abundance decreases rapidly. Beyond 3 R$_*$, one can note a transformation of molecular in atomic Al due to the decreasing gas densities with distance from the star. We have performed an in-depth study of the high spectral resolution optical Mercator/Hermes (Raskin et al. 2011) data of IK Tau and W Hya (no observations are available for R Dor) to check for the presence of atomic Al in the outer atmosphere/inner wind of both stars. Molecular line veiling complicates the analysis of the data. We could not identify either absorption or emission atomic Al lines. This does not imply that no atomic Al is present, but at least the quantity is too low for it to be detected amongst the molecular lines. An analogous conclusion was drawn by Kamiński et al. (2016) for the low mass-loss rate AGB star o Cet, for which reason they concluded that Al is locked in molecules and dust.

This ensemble of considerations supports the conclusion that only a minor fraction of Al resides in Al-bearing molecules and that the atomic Al abundance is difficult to constrain. An important outcome from these ALMA data is that the aluminium condensation process, considered to be the first condensation cycle to start in AGB stars (Tielens 1990), is for sure not fully efficient since the gaseous precursors of the aluminium grains are detected in and beyond the dust formation region.

4.2. Aluminium depletion into grains

Presolar grains prove that aluminium oxide grains are formed in oxygen-rich AGB stars. The circumstellar Al$_2$O$_3$-grains are relatively abundant in meteorites (Nittler et al. 1997), albeit perhaps not as abundant as one would expect if all aluminium would
condense in these grains (Alexander [1997]). This result from meteorite studies now gets some support by our analysis of the ALMA data, confirming that a fraction of the aluminium is still present in its gaseous form after its passage through the dust formation region. At least for a few silicate grains, the meteoric studies show that the aluminium oxides are at the core of the silicate grain suggesting that Al$_2$O$_3$ is the first solid to form in the CSE (Nittler et al. [2008], Vollmer et al. [2006]). Both crystalline and amorphous Al$_2$O$_3$ enclosures have been detected (Stroud et al. [2004]). The variation in the crystal structure and Ti content of these presolar grains demonstrate that Al$_2$O$_3$ can condense in the absence of TiO$_2$ seed clusters but that Ti may be important in determining the lattice structure.

Fig. 17. Predicted abundances of aluminium-bearing molecules with respect to the total gas number density as a function of phase φ for three specific radii (top: 1 R$_\star$, middle: 3 R$_\star$, bottom: 5 R$_\star$). Chemical models are based on the pulsation-induced shock dynamics presented by Gobrecht et al. [2016] for a star resembling IK Tau.

The SED analysis of R Dor and W Hya turned out to be challenging in terms of the aluminium content (Khouri et al. [2015], Khouri [2014]). Based on constraints from gas-phase models and solar abundances, Khouri et al. were unable to model the SEDs of both stars in the spectral region around 11 µm when considering aluminium condensates only to be present in the stellar outflow (see dotted line in Fig. 18). One can fit the broad 11 µm feature in the SED by invoking the presence of a gravitational bound dust shell (GBDS; see Sect. 2.3 for a more detailed explanation on this terminology) of amorphous Al$_2$O$_3$ grains at ∼2 R$_\star$ (see dashed line in Fig. 18). The GBDS can contain both small and large Al$_2$O$_3$ grains. The model for R Dor (W Hya) requires an Al$_2$O$_3$ dust mass in the GBDS of ∼5.7 × 10$^{-10}$ M$_\odot$ (∼1.5 × 10$^{-9}$ M$_\odot$), which would correspond to a gas mass of 7.5 × 10$^{-6}$ M$_\odot$ (2 × 10$^{-5}$ M$_\odot$) if one would assume full aluminium condensation. If this is compliant (or not) with the total aluminium content is difficult to assess since the region where the GBDS resides is known to be highly variable in density due to the stellar pulsations, with variations up to one order of magnitude (Höfner et al. [2016]).

Polarized light data confirm also the presence of large grains close to W Hya and R Dor at 1.5–3 R$_\star$ (Norris et al. [2012], Khouri et al. [2016], Ohnaka et al. [2016]). From the scattered light data, one can not determine the composition of the grains, and both aluminium oxide grains and cold Fe-free silicates are suggested to be good candidates due to their glassy character (Sect. 2.3).

The GBDS results (Khouri [2014], Khouri et al. [2015], the scattered light data (Norris et al. [2012], Khouri et al. [2016], Ohnaka et al. [2016]), the interferometric results (Zhao-Geisler et al. [2015]), and the theoretical models (Höfner et al. [2016]) build up evidence for a shell of aluminium oxide grains at 1.5 – 3 R$_\star$. The kinetic temperature in that region is around 1500–2000 K. Optical constants are measured for amorphous Al$_2$O$_3$ grains, but only for wavelengths beyond 0.2 µm (Koike et al. [1995]) or beyond 7.8 µm (Begemann et al. [1997]). Depending on the replica used for the short-wavelength range and under the
assumption of thermodynamic equilibrium, the estimated temperature of the amorphous alumina grains at that spatial region would be around 1200–1600 K (Khoury et al. 2015). However, amorphous alumina can only exist below 1000 K (Levin et al. 1998; Levin & Brandon 2005). At temperatures around 1500 K, crystalline α-alumina can form, while below 1300 K crystalline γ-alumina can exist. With the grain temperature in the 1.5–3 R̃ region being higher than the annealing temperature, this would imply a structural transformation of Al₂O₃ to its crystalline form. The thermal infrared spectrum of R̃ Dor and W Hya is not compatible with the presence of Al₂O₃ grains with a crystalline γ-lattice structure (see Fig. 13). As shown in Fig. 13 crystalline α-Al₂O₃ can indeed explain the 13 μm feature in the SED. A crystallinity degree of 5% can explain the 13 μm feature in W Hya, while for R̃ Dor the estimated crystallinity degree is around 12%. These crystalline grains might be the scattering agents of the polarized light emission.

However, this questions how to explain the broad 11 μm feature in the SED of R̃ Dor and W Hya and, in particular, the MIDI data of W Hya which clearly show that emission arises very close to the star. A potential answer to that question is that the 11 μm feature does not signal the presence of solid-state amorphous aluminium oxide, but — to the contrary — points towards the existence of large neutral gas-phase aluminium oxide clusters (see Sect. 4.3). Individual (Al₂O₃)ₙ clusters may exist above 1500 K. We note that our analysis does not exclude the existence of amorphous aluminium oxides in the wind, but only at larger distances from the star where temperatures are cooler.

4.3. Constraining the presence of aluminium oxide clusters

If amorphous alumina dust grains are not the carrier of the MIDI and ISO spectral signature at 11 μm, then the interesting possibility exists that large aluminium oxide clusters are present, and detected, just above the stellar surface. Indeed, an outcome of the experimental IR-REMPI studies by van Heijnsbergen et al. (2003) is that large AIO-(Al₂O₃)ₙ, clusters (n > 34) exhibit a spectral signature that is very similar to that of amorphous Al₂O₃, but smaller AIO-(Al₂O₃)ₙ clusters (around n = 15) show the best match with that of crystalline γ-Al₂O₃ (see Fig. 19). Due to the non-linear regime in which the IR-REMPI results are obtained, one can however not estimate the amount of clusters present in the beam. This renders the impossibility of quantifying the amount of large aluminium oxide clusters that would be needed in order to explain the 11 μm feature.

If the 11 μm feature marks the presence of large (n > 34) aluminium oxide clusters, then one should wonder if smaller clusters are present as well and if they can be detected. The experiments by van Heijnsbergen et al. (2003) and Demyk et al. (2004) show that clusters with n = 15–40 show two vibrational bands, one around 11.8 μm and another around 15 μm. Comparing this to the emission features of solid-state aluminium oxide lattices identifies these gas phase clusters to have a structure similar to crystalline γ-Al₂O₃ instead of α-Al₂O₃ (corundum), which is the thermodynamically most stable form of the bulk (see Fig. 19). The infrared observations of W Hya and R̃ Dor do not display an obvious emission component around 15 μm. This does not imply by necessity that these n = 15–40 sized clusters are not present, but at least they are not abundant enough to leave any spectral imprint.

Due to variety of processes prevalent in the vast interstellar space such as collisions, condensation, coagulation, coalescence, the size distribution of interstellar dust grains is dominated by small particles, i.e. n_{2}(a) \propto a^{-7/2} da (Mathis et al. 1977). Also in our own Earth’s atmosphere, fresh aerosols which are created in situ from the gas-phase by nucleation display a number distribution heavily skewed towards the very small particles (Seinfeld et al. 1998). In analogy, one might expect a significantly larger fraction of very small aluminium oxide clusters as compared to large clusters in the stellar wind. Current capacities in quantum chemical computations give us the possibility to test this proposition on the prevailing presence of very small clusters; see next section.

4.3.1. Emission of very small (Al₂O₃)ₙ (n ≤ 4) aluminium oxide clusters

A way to test if very small Al₂O₃ polymers are present is via the detection of their vibrational frequencies. These bands arise owing to the presence of internal bending and stretching modes in the cluster. As the energy and geometry, the vibrational spectrum differs from isomer to isomer, and thus can be seen as a spectral fingerprint.

Because there is no way to currently predict the most likely cluster composition in the outflow and because these clusters would probably range over a wide range in both stoichiometry as well as atomic sizes, we have taken the simple approach of calculating the spectral properties of a range of stoichiometric alumina clusters to estimate where observable lines might exist. For n = 1–4 we have determined the most stable structures of the neutral aluminium oxide clusters using density functional theory (DFT); see Fig. 20. The computations were accomplished by the GAUSSIAN 09 package (Frisch et al. 2009) using the hybrid B3LYP (Becke, three parameter, Lee-Yang-Parr; Lee et al. 1988)
The predicted spectra compare well with the experimental results by Demyk et al. (2004) and the calculated linear infrared absorption spectra by Stierka et al. (2007) for small cluster sizes (see Fig. 31), with the strongest peaks in the 10-11 \( \mu m \) region and an ensemble of smaller peaks around 14 \( \mu m \). Implementing the stable clusters in thermo-chemistry calculations for densities down to \( 1 \times 10^{-4} \) dyne cm\(^{-2} \) (H"ofner et al. 2016) and temperatures up to 1800 K and allowing the small clusters to grow via monomer addition indicates that (Al\(_2\)O\(_3\))\(_3\) seems to be the best candidate for possible detection in CSEs (see Table 4).

We have tested if the spectral features present in the infrared SED of R Dor and W Hya could be explained by the vibrational frequencies of these small aluminium oxide clusters (see Fig. 22). However, the low spectral resolution (around 300) of the ISO/SWS speed 1 data for both stars makes it impossible to draw any firm conclusion. Albeit a positive correlation can be noticed between various absorption peaks in the ISO data and the predicted cluster spectra, we caution against over-interpretation of these results. Specifically, molecular line veiling by other molecules which might be present in the `extra-molecular` layer created by pulsation-induced density enhancements result in an ensemble of emission and absorption features that complicates any potential identification. High spectral resolution data in the 10-20 \( \mu m \) regime (as might be obtained in the future using the E-ELT/METIS instrument) is paramount to answer the question on the potential presence and vibrational excitation of these small aluminium oxide clusters.

The more pronounced evidence of large (\( n > 34 \)) (Al\(_2\)O\(_3\))\(_n\)-clusters (Fig. 19 and Fig. 13) warrants a discussion on the possibility if a physico-chemical situation might occur resulting in a skewed cluster-size distribution toward large cluster sizes.

### 4.3.2. Skewed cluster-size distribution

First of all, one might wonder if the grain-size distribution in the inner wind region of AGB stars is similar to the one found in the ISM, \( n_d(a) \propto a^{-\frac{7}{2}} \) (Mathis et al. 1977), Dominik et al. (1989) derived a particle size distribution for carbon-rich stars with spectral index of ~5 using Classical Nucleation Theory (CNT) with heteromolecular homogeneous grain formation as developed by Gail & Sedlmayr (1988). A different approach was pursued by Gobrecht et al. (2016) who included pulsation-induced shocks in the inner wind of an oxygen-rich AGB star and assumed coalescence and coagulation of (molecular) dimers to form dust grains. Using a Brownian formalism to compute the grain size distribution, they showed that coagulation is only efficient for dust growth for late phase (\( \phi > 0.8 \)), resulting in very small aluminium oxide grains in the size range of 7–20 nm after one oscillation. Assuming that the aluminium oxide grains survive the next passage of the periodic shocks and that growth occurs through surface deposition gives rise to a grain size distribution at 2 stellar radii after 12 pulsation cycles with two components, one peaking at ~30 nm, the other around 300 nm. This result is already a first indication that size distributions in CSEs might differ from the ISM characteristics mentioned above.

Two direct pathways for clusters to grow is via adding monomers and by collisions and sticking together. Since the number of seeds is low, the chance of collision with monomers will be higher than of collision with larger polymers, so the first pathway seems to be preferred. The region around 2.5R* coincides with the GBDS, i.e. a higher density region where species can stay longer without being pushed outward. This might create a favourable condition for clusters to grow to large sizes. These large aluminium oxides can be very stable at high temperatures due to their ability of undergoing thermo-ionic emission rather than dissociation (Demyk et al. 2004). I.e. the clusters preferentially emit an electron, a unique property which is only observed for very strongly bound species. This ability might also greatly enhance the growth efficiencies of the clusters, since the transient complex that is formed during the growth reaction process might also stabilize via the emission of an electron.

Growth by adding monomers is hence a potential process for the creation of larger clusters, with a preference for specific cluster sizes initiating coagulation. Energy considerations in this highly turbulent region just above the stellar atmosphere should be taken into account to answer the question on the favourable cluster size for coagulation. No calculations includ-

| \( T \)  | 1000  | 1200  | 1500  | 1800  |
|-------|------|------|------|------|
| 1     | √    | √    | √    |
| 0.1   | √    | √    | √    |
| 0.01  | √    | √    | x    |
| \( 10^{-2} \) | √ | (Al\(_2\)O\(_3\))\(_3\) |
| \( 10^{-4} \) | √ | (Al\(_2\)O\(_3\))\(_3\) |

Table 4. Overview of the alumina nucleation by monomer (Al\(_2\)O\(_3\)) addition at different temperatures \( T \) (in K) and pressures \( p \) (in dyne cm\(^{-2} \)). An energetically feasible nucleation is marked with √. Suppressed nucleation with (large) energy barriers is marked with x. If the nucleation pathway is partially favourable, the largest preferential cluster is given.

\( \text{[1988]: Miehlhich et al. 1989: Becke 1993} \) exchange-correlation functional with a 6-31+G* basis set. The binding energy and stability of electronic systems including clusters are pressure and temperature-dependent, respectively. Variations in temperature and density imply that the energy levels of the clusters may shift and that the order of the most stable clusters may change. We have calculated how the stability\(^5\) of the considered small alumina clusters is affected in various ways for conditions occurring in the CSE (with pressure \( p = 0.001 – 50 \text{ Pa} \) and temperature \( T = 500 – 3000 \text{ K} \)). For Al\(_2\)O\(_3\), the first excited structural isomer is a linear chain and has a potential energy 0.1 eV above the kite-shaped triplet ground state. Above 1000 K the linear form is slightly more stable, below 1000 K the kite-shaped triplet structure is favoured. Considering (Al\(_2\)O\(_3\))\(_2\), the energy difference of the ground state to the first excited state is relatively large (0.48 eV) and therefore structure 2A (see Fig. 1 in Li & Cheng 2012) is also the most stable in circumstellar conditions. For \( n = 3 \), we find five stable structures in an energy interval of only 0.13 eV for the alumina trimer. In circumstellar conditions, however, the first excited state 3B (Li & Cheng 2012) is the most stable configuration. For a temperature of 1500 K, the ground and first excited state of (Al\(_2\)O\(_3\))\(_4\) are almost identical in potential energy. Below 1500 K isomer 4A is favoured, above 1500 K structure 4B (Li & Cheng 2012) which is only stable for pressures above 0.1 Pa. Overall, the Gibbs free energy of formation for alumina clusters depends significantly on \( T \), but not much on density or pressure.

\(^5\) Calculated from the Gibbs free energy. The entropy is given by the partition function (with contributions from electronic, translational, vibrational and vibrational motion) of which the translational part depends on the pressure.
including only a substantial quantity of large metal clusters can be formed and grains and subsequently ejected. Nozzle experiments show that ing which large clusters are formed on the surface of existing face processes; i.e. a heterogeneous nucleation process dur-
ways. One possibility is the formation of large clusters by sur-
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sume that these are in fact present, as indicated by the observed then we would not expect to see (much) large clusters, but we as-
phase. If coagulation were to commence from small cluster sizes,
byStranz (1980) shows that SiO monomers, dimers and trimers is noted for (SiO)
clusters show indeed
clusters are currently available to answer this question. Gener-
starting at rather small cluster sizes (\(n\) = 3, 4). Our calculations including only the \(n = 1 - 4\) (Al\(_2\)O\(_3\))\(_n\) clusters show indeed a preference for the \(n = 3\) cluster size. A similar behaviour is noted for (SiO)\(_n\), for which the matrix isolation experiment byStranz (1980) shows that SiO monomers, dimers and trimers can be seen, but then the material seems to transition to the bulk phase. If coagulation were to commence from small cluster sizes, then we would not expect to see (much) large clusters, but we assume that these are in fact present, as indicated by the observed 11 \(\mu\)m spectral feature.

Large clusters could, however, be formed by alternative pathways. One possibility is the formation of large clusters by surface processes; i.e. a heterogeneous nucleation process during which large clusters are formed on the surface of existing grains and subsequently ejected. Nozzle experiments show that a substantial quantity of large metal clusters can be formed and ejected that way (Knauer 1987). The NACO and SPHERE data prove that grains (of still unknown composition) are ubiquitous close to the star. These grains might serve as surface for cluster growth to occur. Vaporization of solid material might offer another explication for a skewed cluster-size distribution toward large sizes. The Al\(_2\)O\(_3\) grain temperatures in the region around 2 R\(_*\), are high (Sect. 4.2) and might lead to the crystallization of the bulk material. If energetically favourable, the material might also partly get vaporized producing large clusters. This kind of behaviour is noted during formation kinetics experiments and computer simulations for the nucleation and growth rates of metal vapors (Yamada et al. 1987). The recent SPHERE data of Khouri et al. (2016) show that the solid-state material is grouped into irregular, clumpy structures. Backwarming occurring between the dust clumps and the star might locally increase the temperature (Fleischer et al. 1995), favouring vaporization to take place.

5. Conclusions

In this paper we have studied the aluminium content in a low and a high mass-loss rate oxygen-rich AGB star, R Dor and IK Tau respectively. The aim was to reveal the role of aluminium species in the initiation of the stellar wind. We therefore have observed both stars with ALMA at high spatial resolution (\(\sim\)150 mas) to trace the dust formation region via aluminium bearing molecules (AlO, AlOH, and AlCl). The azimuthally averaged flux densities in function of the angular distance from the central star were fitted using a non-LTE radiative transfer code to retrieve the fractional abundances of the molecules. The gas-phase aluminium chemistry is largely different for both stars, in particular the AlO and AlOH fractional abundances. In IK Tau AlOH is clearly detected, while traces of clumpy structures containing AlO are only apparent beyond 50 R\(_*\). In contrast, AlO is \(\sim\)70 times more abundant than AlOH in R Dor. These three molecules consume only \(\lesssim\)2% of the total aluminium budget. Hence, there is ample opportunity to form aluminium-bearing dust species. AlO and AlOH are direct precursors of these aluminium-bearing grains and both molecules are detected well beyond the dust condensation radius. This implies that the aluminium dust condensation cycle is not fully efficient.

To assess the aluminium dust content in oxygen-rich AGB stars, we have also included the well-studied low mass-loss rate
Fig. 22. Upper panel: normalized opacity of the \((\text{Al}_2\text{O}_3)_n\) clusters convoluted with a Lorentzian profile with a FWHM of 0.03 \(\mu\)m. The full coloured lines represent the opacities normalized for each cluster entity separately (with the same colour coding as in Fig. 20), while the dotted coloured lines indicate the wavelength position of all ground-state vibrational frequencies of the stable \((\text{Al}_2\text{O}_3)_n\) \((n = 1 - 4)\) clusters. Middle panel: Comparison between the (stellar continuum subtracted and normalized) SED of R Dor (full black line) and W Hya (full gray line) with the predicted vibrational frequencies of the stable \((\text{Al}_2\text{O}_3)_n\) \((n = 1 - 4)\) clusters (vertical coloured lines). Grey areas indicate the region with some of the largest \((\text{Al}_2\text{O}_3)_n\) opacities. Dashed gray lines indicate the CO\(_2\) lines as discussed by Justtanont et al. (2004). The full red line is the (stellar continuum subtracted and normalized) emission for a slab model containing H\(_2\)O, SiO, and SiS. Column density for all species were taken to be \(1 \times 10^{20}\) cm\(^{-2}\) at 0.5R\(_*\) above the stellar surface for a temperature of 2000 K. The individual contributions of H\(_2\)O, SiO, and SiS are shown in the bottom panel. Note that the column densities of the molecules were not chosen to fit the ISO/SWS data, but serve as illustrative examples on the molecular line veiling.
star W Hya. We discuss how the spectral features present in the spectral energy distribution (SED), polarized light signal, and interferometric data point toward the presence of a halo of large (and small) transparent grains close the star. A candidate species for these grains is amorphous Al$_2$O$_3$. However, at a distance of only 1.5 R$_*$, the estimated grain temperature is > 1000 K, i.e. too high for the grains to retain their amorphous lattice structure. The grains should anneal and form a crystalline compound. Indeed, the typical 13 $\mu$m features signalling the presence of crystalline Al$_2$O$_3$ (n-Al$_2$O$_3$) is seen in the SEDs of W Hya and R Dor. One is then left with the question how to explain the broad 11 $\mu$m feature in the SED and interferometric data. We propose that large gas-phase (Al$_2$O$_3$)$_n$-clusters (n > 34) are the species that produce the signatures seen in the SED and interferometric data. We explain how these large clusters can be formed. Using density functional theory (DFT) we calculate the stability and emissivity of very small clusters (n ≤ 4). We show how future E-ELT/METIS observations will be crucial to answer the question if very small clusters (n ≤ 4) are present in the inner winds of these oxygen-rich AGB stars.

Acknowledgements. LD acknowledges support from the ERC consolidator grant 646758 AEROSOL and the FWO Research Project grant G024112W. We acknowledge the CINECA award under the ISCRA initiative for the availability of high performance computing resources and support. This paper makes use of the following ALMA data: ADS/JAO.ALMA2013.0.0166.S. ALMA is a partnership of ESO (representing its member states), NSF (USA) and NINS (Japan), together with NRC (Canada) and NSC and ASIAA (Taiwan), in cooperation with the Republic of Chile. The Joint ALMA Observatory is operated by ESO, AU/NRAO and NAOJ. We thank Willem Jan de Wit for his contribution to the reduction of the VLTI/MIDI data of R Dor. We acknowledge with thanks the variable star observations from the AAVSO International Database contributed by observers worldwide. Based on observations obtained with the HERMES spectrograph, which is supported by the Research Foundation - Flanders (FWO), Belgium, the Research Council of KU Leuven, Belgium, the Fonds National de la Recherche Scientifique (F.R.S.-FNRS), Belgium, the Royal Observatory of Belgium, the Observatoire de Genève, Switzerland and the Thüringer Landessternwarte Tautenburg, Germany.

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