An Effective Power Tracking Algorithm for Partially Shaded Solar PV Array Employing Micro Converters Feeding to DC Microgrid

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Abstract
This paper proposes the analysis of power enhancement in partially shaded PV system supplying DC microgrid employing micro converters with a modified Perturb and Observe (P & O) based on Maximum Power Point Tracking (MPPT) technique by sensing the load parameters alone. The proposed technique is effective in power tracking under both normal and partially shaded conditions with the reduced number of sensing devices as compared to those used in the conventional DMPPT (Distributed Maximum Power Point Tracking) techniques. In this work, two series configured micro converters are considered for supplying 120 V DC microgrid from partially shaded PV panels. The complete steady-state analysis is developed and predicted the performance of the proposed MPPT operation and compared with the simulation and experimental results. The PV panels are emulated in the experiments. The effectiveness of the proposed technique is demonstrated and substantiated by theoretical, simulation and experimental results under various operating conditions.

Keywords
PV system, MPPT, micro converters, DC-DC converter, DC microgrid, DMPPT, cascaded converters and distributed generation

1 Introduction
The continuously increasing power demand is met by both the conventional and renewable electric power generation sources. Most of the countries have modified the electric system in order to establish the microgrids with the Distributed Generators (DGs) [1, 2]. The DGs are located close to the load centers [3, 4] which will reduce the cost and energy loss of the transmission system. Among the DGs, solar PV and wind energy sources are the major power resources. The solar PV has remarkable technological developments due to the advantages such as less maintenance, reliability and integrability. In general, the PV power may be directly fed to the stand-alone/grid connected applications with DC-DC/DC-AC power converters. Due to the nonlinear characteristic, behavior of PV module, extracting the maximum power is a challenging task. In this regard, various MPPT techniques are proposed in the literatures [5–7].

In general, Partial Shading (PS) occurs in the solar PV module due to clouds, trees, buildings and overhead wires. Extracting the maximum power under PS conditions is considerably complex compared to that in the uniform shaded conditions. In particular, the output power of series connected PV module is significantly influenced with the PS condition [8] and creates local hotspots in unshaded panels. In such situations, the conventional MPPT algorithms are ineffective [8]. Using of bypass diode [8–11] the complete Partial Shading effect can be eliminated from the series connected PV panels. However, the PS PV modules become ineffective and multiple peaks will occur in the PV characteristic. For tracking maximum power under PS PV panels, various "global" MPPT (GMPPT) techniques have been proposed [10–14]. These strategies increase the over-all power yield but leads to complete loss of power from a PS module.

Further, to address the effect of PS and GMPPT, a micro level converter is interfaced in each PV module supplying grid connected/stand-alone loads based on the cascaded connection of micro converters.

In this scheme, the tracking of MPP of each PV module in the string is called as Distributed Maximum Power Point Tracking (DMPPT) [15, 16]. This solution is powerful under...
PS conditions compared to the array level (GMPPT) configuration employing centralized power converter. There are two DMPPT configurations available based on the system composed of the PV module with the DC-DC converters. In the first configuration, the output of the PV module is connected to the input of the DC-DC converter and its output is connected in series. In this configuration the DC-DC converter tracks the full power of each PV module and it name as Full Power DC-DC (FPDC) converter [17]. In the second configuration, the output of the PV module is connected to the DC-DC converter output terminals and its input terminals are connected in parallel. In this configuration the DC-DC converter tracks maximum power based on the current compensations and is called as Compensation Power DC-DC (CPDC) converter [18]. Recently, [19, 20] have developed DMPPT technique for both FPDC and CPDC configuration and the MPPT is attained by sensing PV parameters such as $v_p$ and $i_p$. These methods require more number of sensors because of each PV panel requires one voltage sensor and one current sensor.

A power electronics equalizer concept is proposed in [21] for DMPPT operation, which requires ten power diodes, eight power switches and one inductor for a 4-module string. This is an inventive scheme, but the controller operation is more complex because of more power devices in this scheme.

A simple Energy Recovery scheme [22] is proposed for tracking maximum power under partial shaded condition. In this scheme a trigger circuit is required to select the shaded module and trigger the power processing circuit. This controller increases the computational process because two different control loops are required for regulating the bus voltage, and the distributed power processing converters, respectively, and also the number of sensing devices is more.

A shunt-series compensation scheme [23] is proposed for fly back converter to track maximum power under partial shaded conditions. In this scheme, the load/grid is disconnected from the input when extracting the MPP information from each module. In [24] a granular control is developed for PV arrays by sensing the output parameters. In this controller MPPT is achieved by varying the duty ratio of each converter based on output power. Due to sensing of output parameters, it requires less number of sensors but the main drawback is that it takes more time to track maximum power under partial shaded condition. A multi-winding forward-based converter developed with a current balancing DPP converter in [25] (CBC) to implement DMPPT technology at module-level and maximize the output power of the PV string during Partial Shading conditions. This method requires more number of sensing devices because of each PV panel requires one voltage sensor and one current sensor. In [26] energy management and control strategy of the DC microgrid system based on the DMPPT control technique. This paper describes the energy management by considering different source with conventional DMPPT technique and it requires more number.

The present paper develops a modified P & O algorithm based on approach given in [24] for the operation of partial shaded solar PV system supplying DC microgrid by sensing the output parameters. Series connected boost derived micro converters are considered for the steady-state and dynamic behavior of the solar PV system under PS conditions. The performance of the system with the proposed controller is demonstrated by simulating the system in MATLAB/Simulink and the prototype of the system has been implemented in the laboratory using a dSPACE real time controller. The efficacy of the proposed controller with a reduced number of sensing devices is verified through simulation and hardware results under various operating conditions of the solar PV system. A steady state analysis has been developed for the chosen configuration and from the steady state plots, it is observed that the proposed DMPPT controller is operating desired MPPT conditions even under varying irradiation and degradation. The paper is organized as follows: the structure, the controller operation and the steady-state analysis of series configuration of PV topology are described in Section 2; the simulation results of the series configuration under PS and degradation conditions are explained in Section 3 and the Section 4 furnishes the details of experimental investigation. The concluding remarks are summarized in Section 5.

2 Power circuit configuration

Fig. 1 shows the generalized schematic representation of a solar PV system with the proposed controller. The power is processed independently for each solar PV module supplying DC microgrid employing series connected micro converters. The proposed technique is capable of operating both in normal and partially shaded PV condition with the reduced number of sensing devices. For example, "n" number of PV modules requires "n" number of DC-DC converter, "n − 1" voltage sensors and one current sensor.
2.1 Controller strategy

The complete generalized control structure for the MPPT operation of solar PV system employing series connected micro converter is shown in Fig. 1 (b). This control technique requires only load parameters such as \(v_{01}, v_{02}, \ldots, v_{0n}\), and \(i_0\). For considering fixed DC microgrid voltage requires \(n - 1\) voltage sensor and one current sensor, whereas the conventional methods require \(2n\) voltage sensors and \(2n\) current sensors. The sequence of proposed MPPT operation is explained using a flow chart as shown in Fig. 2. In which, the conventional P & O algorithm is modified to enhance the PV power generation effectively under PS conditions. To validate the performance of the proposed technique, two PV modules are considered with two series connected micro converters interface supplying DC microgrid with one voltage sensor and one current sensor. Performance prediction of the proposed control technique is observed by initially assigned with the duty ratio of each converter and the output power of each converter and the value of \(a\) are observed. Here, \(a\) is the output of the \(n + 1\) AND gate, its inputs are outputs of 1 to \(n\) AND gates. The digital logic circuit implementation for identifying the PS modules is shown in Fig. 2. If \(a\) equal to zero, indicates that the PV modules are partially shaded and the proposed control technique works as a modified P & O algorithm. This will reduce the duty ratio of the corresponding shaded PV panel converter and increases the duty ratio of the non-shaded PV module converter based on the conditions given in the flow chart as shown in Fig. 2. This sequence contentious till all the converters reach their maximum powers. If the value of \(a\) equals 1, which means no shaded on the panels at this condition the proposed technique works similar to conventional P & O algorithm [5]. The complete steps of the modified P & O algorithm are given in Fig. 2.

In the proposed modified P & O algorithm, the frequency of perturbations, or the time interval \(t_a\) between two consecutive perturbations, and their amplitude must be carefully chosen to optimize the dynamic performances and the steady-state efficiency of the MPPT algorithm. The value of the parameter \(t_a\) must be selected on the basis of the DC-DC converters dynamic behavior [5]. In this paper, the settling time of the response of the DC-DC converters output current to a step variation of the duty cycle is evaluated. Consequently, the optimal \(t_a\) value does not change when a classical Single Variable (SV) P & O algorithm or the proposed algorithm is used. In this, \(t_a = 1\) ms which is equal to 1000 Hz of execution frequency. Whereas in case of \(\Delta D\), the above conclusion cannot come because the oscillations of the outputs around the steady-state values depend on \(\Delta D\). A small step size will take more time to reach MPP or it may oscillate around the reference voltage in the case of high step size. Due to this, an optimal \(\Delta D\) must be chosen.
The optimum value of $\Delta D$ is calculated using the following expression

$$\Delta D = \frac{1}{G_0} \sqrt{\frac{N \, N_{cell} \, K \, \Delta S \, t_s}{H \, V_{mpp} + \frac{1}{R_{mpp}}}},$$

where $G_0$ is the reference irradiation, (1000 W/m$^2$), $N$ is number of DC-DC converters, $V_{mpp}$ is maximum PV voltage at 200 W/m$^2$ (27.65 V), $K$ is a coefficient proportional to derivative of the PV current with respect to the irradiance, ($6.895 \times 10^3$, Am$^2$/W), $R_{mpp}$ is the differential resistance of the PV module evaluated in its MPP, $H$ is a coefficient proportional to the second derivative of PV current with respect to the PV voltage ($5.9 \times 10^4$, A/v$^2$), $DS$ is constant rate of change equal to 50 W/m$^2$s. The optimum value of $DD$ from the above values is 0.00241.

### 2.2.1 Performance of PV panels

The performance of the PV panels is analyzed with the mathematical modelling given in [27, 28]. A PV cell is modeled as a current source shunted with a diode and represented by an equivalent circuit [27] shown in Fig. 3. The characteristics of the panel are obtained by connecting a number of such cells in series. The equation relating the output current and the voltage of a PV module can be written as

$$I_{pv} = I_{ph} - I_{sat} \left\{ \exp \left[ \frac{V_{pv} + I_{pv} \, R_s}{n \left( \frac{K \, T_c}{q} \right)} \right] - 1 \right\} \frac{V_{pv} + I_{pv} \, R_s}{R_s},$$

$$T_c - T_a = \frac{NOCT - 20}{800} \times G_0.$$ 

### 2.2 Steady state analysis

The steady-state analysis of the system considered is organized into two parts. Firstly, the performance of the PV panels are analyzed under various operating conditions and secondly, the mathematical analysis of the boost derived DC-DC converter is developed.
The following steps give the complete detail of PV panel performance.

Step 1: Calculate the junction temperature $T_c$ using the Eq. (2).

Step 2: Calculate the saturation current $I_{sat}$ and the photocurrent $I_{ph}$ using the Eq. (4) and Eq. (5)

$$I_{sat} = \exp \left( \frac{q \times V_{oc}}{nKT_c} \right) - \exp \left( \frac{q \times I_{sc} \times R_s}{nKT_c} \right)$$

$$I_{PV} = I_{sat} \left[ \exp \left( \frac{V_{PV}}{n(KT_c/q)} \right) - 1 \right] - \frac{V_{oc}}{R_{sh}}$$

Step 3: Solve the Eq. (2) and plot the current-voltage characteristics and the power-voltage characteristics.

Step 4: By using program, it can directly solve the Eq. (2), but in the form of two equations, Eq. (6) and Eq. (7)

$$X(V_{PV}, I_{PV}) = I_{sat} \left[ \exp \left( \frac{V_{PV} + R_s \times I_{PV}}{n(KT_c/q)} \right) - 1 \right]$$

$$Y(V_{PV}, I_{PV}) = I_{ph} \left[ -\frac{V_{PV}}{R_{sh}} - \left( \frac{R_s}{R_p} + 1 \right) \right] \times I_{PV}$$

Step 5: Find the maximum power, then the maximum voltage and the maximum current without calculation.

The meanings of the symbols in Eqs. (2)–(7) are as follows:

$I_{sc}$: short-circuit current (A), $V_{oc}$: open-circuit voltage (V), $R_s$: series resistance (Ω), $R_{sh}$: parallel resistor (shunt) to the diode (Ω), $k$: 1.38 $\times$ 10$^{-23}$ J/K, Boltzmann constant, $q$: 1.602 $\times$ 10$^{-19}$ electron charge (C), $T_c$: junction temperature (K), $n$: ideality factor of the solar cell, between 1 and 5 in practice, NOCT: Nominal Operating Cell Temperature, $T_a$: ambient temperature and $G_0$: irradiance (W/m$^2$).

Fig. 4 (a) and (b) shows the Maximum Power Points (operating points) under different irradiation and series resistance of the PV panels respectively. The MPP operation is obtained by the steps given in the flow chart (Fig. 5).

### 2.2.2 DC microgrid connected boost converter

After calculating the PV operating points, it is of interest to analyze the performance of the boost converter. Therefore, in this section, a technique is developed to find the duty ratio of the micro converter to operate the PV panels at MPP.

### 2.2.3 Cascaded boost converter

The current passing through all boost converters is same and the microgrid voltage is equal to the sum of the individual boost converter voltages.
Considering two boost converters connected in series, the DC behavior of this topology is described by where,

\[ i_{01} = i_{02} = i_0 \]  
\[ i_0 = i_{pv1} \times (1 - D_1) \]  
\[ i_0 = i_{pv2} \times (1 - D_2) \]  
\[ v_{01} = \frac{v_{pv1}}{1 - D_1} \]  
\[ v_{02} = \frac{v_{pv2}}{1 - D_2} \]  

However, for carrying out this analysis, the total converter loss is required and the procedure to calculate the converter loss is depicted in the Appendix A. The total output power is the sum of the input power and the converter losses.

\[ P_{tl} = P_0 + P_{pl} \]  
\[ P_{m} = P_{pv} + P_{pl} \]  

From Eqs. (8)–(17), it can be observed that the values of \( i_0, P_0, \) and \( P_{pl} \) are essential for finding the duty ratios. Initially, the values are not known for the pre-determination process. Hence, a simple technique is designed to find the initial values of \( i_0, P_0, \) and \( P_{pl} \) on the basis of power balance and known parameters (given in the Appendix A). The complete steps for the analysis are given in Fig. 2 for finding the duty ratio.
3 Results and discussion

The complete solar PV system supplying a DC microgrid shown in Fig. 1, has been developed using MATLAB/Simulink toolbox.

The proposed DMPPT operation has been validated for series connected boost derived micro converters under different case studies with a reduced number of sensors. The system parameters considered for these case studies are given in Table 1.

3.1 Steady state performance

The steady state performance of the system with the proposed controller is shown in Fig. 6. Fig. 6 (a) and (b) shows the plots of the operating points ($D_1$, $D_2$, $V_{01}$, $V_{02}$ and $P_0$) with respect to different irradiation and series resistance of PV panels respectively. From Fig. 6 (a) it is observed that, the series configuration with an irradiation less than 400 W/m$^2$ results in a negative duty ratio. Hence, this configuration can only be operated up to 400 W/m$^2$. Further, the closeness of the simulated, experimental and calculated values confirms that the proposed controller is working effectively for both PS and degradation conditions as shown in Fig. 6 (a) and (b).

3.2 Comparison of DMPPT configuration with and without bypass diode configuration

Fig. 7 shows the different configuration under PS condition. In Fig. 8, PV panel 1 has 1000 W/m$^2$ and PV panel 2 irradiation is varying from 1000 W/m$^2$ to 200 W/m$^2$, that is represented as $x$ in the Fig. 7.

3.3 Simulation results

The simulation is carried out to evaluate the proposed controller performance under various operating conditions of solar PV system such as change in irradiation and degradation.

3.3.1 Series configuration

The effect of PS has been studied through simulation with step change in irradiation. In this study, Fig. 1 (a) is considered to validate the controller. Fig. 9 (a) and (b) shows the simulation results of the solar PV system with DMPPT operation. By setting DC microgrid voltage at 120 V and the solar irradiation at 1000 W/m$^2$ from time $t = 0.04$ s to 0.1 s for both the PV panels, the corresponding PV voltages ($v_{PV1} = v_{PV2} = 30.5$ V), currents ($i_{PV1} = i_{PV2} = 8.21$ A) and powers ($P_{PV1} = P_{PV2} = 250.4$ W) are observed. During this duration, it is noticed that, both the converters are sharing the microgrid voltage ($v_{01} = v_{02} = 60$ V). The corresponding

| Table 1 Parameters | Values |
|---------------------|--------|
| Maximum PV voltage  | 30.5 V |
| Maximum PV current  | 8.21 A |
| Inductor            | 1.5 mH |
| Capacitors          | 1000 µF |
| Switching frequency | 20 kHz |
| Micro grid voltage  | 120 V (series) |
Fig. 8 Power–voltage plots of the PV panels with, without bypass diodes and the proposed DMPPT configuration for panel 1 (1000 W/m²), (a) panel 2 (800 W/m²) (b) panel 2 (600 W/m²) (c) panel 2 (400 W/m²) (d) panel 2 (200 W/m²)

Fig. 9 Simulation results: (a) PV voltages, currents and powers (b) converter duty ratio, voltages, currents and powers for series connected boost converters with step change in irradiation in panel 2
current at each converter $i_{01} = i_{02} = 4.09$ A, the power outputs $p_{01} = p_{02} = 245.4$ W and the total power fed to the microgrid terminals is 490.8 W.

Fig. 9 (a) and (b) also shows the performance for the dynamic variation in the irradiation of the solar PV panels. With the same level of microgrid voltage (120 V) and standard irradiation of $(1000 \text{ W/m}^2)$ for panel 1 at time $t = 0.1$ s a step change in irradiation for panel 2 is applied from $(1000 \text{ W/m}^2$ to 800 W/m$^2$). In this duration, the PV panel voltages ($v_{pV1} = 30.5$ V and $v_{pV2} = 30.1$ V), currents ($i_{pV1} = 8.21$ A and $i_{pV2} = 6.53$ A), powers ($p_{pV1} = 250.4$ W and $p_{pV2} = 196.5$ W) together with power supplied to the DC microgrid (446.9 W) are observed. Further, the DMPPT controller adjusts the duty ratio to the desired value ($D_1 = 0.491$ to 0.544 and $D_2 = 0.491$ to 0.431) under varying irradiation to maintain the constant value of the output current (3.63 A) of the series converters. Further, it is observed that the converter 1 voltage is raised to 67 V and converter 2 is dropped to 53 V. Similarly, at time $t = 0.2$ s the step change in irradiation for panel 2 is reduced from 800 W/m$^2$ to 600 W/m$^2$. In this duration, the PV panel voltages ($v_{pV1} = 30.5$ V and $v_{pV2} = 29.4$ V), currents ($i_{pV1} = 8.21$ A and $i_{pV2} = 4.92$ A), powers ($p_{pV1} = 250.4$ W and $p_{pV2} = 144.6$ W) and power fed to the DC microgrid are observed. The duty ratio of each power converter ($D_1 = 0.544$ to 0.598 and $D_2 = 0.431$ to 0.331) is adjusted by the controller to maintain the constant value of the converters output current (3.22 A) to ensure DMPPT operation. The results show that the converter 1 voltage raised to 76 V and converter 2 voltage dropped to 44 V.

### 3.3.2 Degradation of the panels

The effect of the degradation in the PV module is a gradual drop in output power over time [29], [30].

This is because of:
1. increases in $R_s$ and
2. reduction in $R_{sh}$.

By considering the degradation in the module, a dynamic simulation study has been performed with the series connected configuration to validate DMPPT operation.

In this case, the step change in $R_s$ in the PV modelling is considered and the corresponding dynamic simulation results are given in Fig. 10. From this figure, it is noticed that for any change in $R_s$, the duty ratio ($D_1 = 0.493, 0.527$ and 0.536 and $D_2 = 0.493, 0.557$ and 0.588) is adjusted by the controller to maintain the output currents ($i_{01} = i_{02} = 4.06$ A, 3.53 A and 3.3 A). Also, the corresponding variation in the converter output voltage sums up to the DC microgrid voltage to validate the correctness of the controller operation.
3.4 Comparison of the proposed controller with conventional controller

To demonstrate the superiority of the proposed controller it is compared with the conventional controller and the comparison results are shown in Fig. 11 (a) and (b). It can be observed from these figures that the proposed controller is effectively tracking the maximum power under the shaded condition similar to the conventional controller. But the conventional controller requires additional sensors compared to the proposed controller. The complete result and sensors requirement are given in Table 2. From this table it is observed that the proposed controller requires only one voltage and one current sensor whereas the conventional controller requires two voltage and two current sensors in case of two series connected micro converters.

Table 2 Performance evaluation of proposed with conventional controller

| Controller   | No. of converters | sensors voltage | sensors current | MPPT | Setting (ms) |
|--------------|-------------------|----------------|----------------|------|--------------|
| Proposed     | 2                 | 1              | 1              | yes  | 30           |
| Conventional | 2                 | 2              | 2              | yes  | 30           |

4 Experimental results

The series connected two DC-DC converters are fabricated using IGBT (IRGT1090U06) switches, diodes (IXYS DSEI30–06A), 1.5 mH inductor and 1000 mF capacitors. The proposed modified P & O algorithm has been implemented in the dSpace DS1103 prototyping platform by programming in the MATLAB/Simulink environment. Gating pulses were generated by using the dSpace platform. The $V_{pv}$ and $P_{pv}$ were averaged over a 10 ms interval and the MPPT control is run every 1 ms. A solar PV module with a $P_{MPP} = 250$ W, $V_{MPP} = 30.5$ V and $I_{MPP} = 8.21$ A is emulated in the 2 kW Chroma solar simulator 62020H-150S [Chroma (2014)]. Hall effect voltage transducers and current sensors were used to sense output voltage and output currents of the converters. Also, a Digital Storage Oscilloscope (DSO) is used to captured the experimental results. Two gate drive circuits with galvanic isolation have been fabricated using the FOD3182SDV [On Semiconductor (2011)] optocoupler and the TMH1215D [Traco Power (2011)] isolated DC-DC converter chip. The schematic of the fabricated gate drive circuit drawn in Kicad-Eeschema. The complete experimental set up shown in Fig. 12.
Fig. 13 shows the experimental results of the PV system with DMPPT operation and for a DC micro grid voltage of 120 V. From Fig. 13, it is observed that up to $t = t_{p1}$ [s] both panels are unshaded (1000 W/m²) and the results of panel voltage, current, power, duty ratio, converter voltage, current and power are shown. At $t = t_{p1}$, the panel 2 is partially shaded (800 W/m²) and panel 1 remains unshaded (1000 W/m²). It is observed that converter 1 voltage is increased, and converter 2 voltage is decreased with respect to duty ratio to maintain the same current at both the converters.

Similarly at $t = t_{p2}$ [s], the panel 2 is further partially shaded (600 W/m²) and the converter 1 voltage is increased and converter 2 voltage is decreased with respect to duty ratio for maintaining the same current at both the converters. From the results shown in Fig. 13, it can be observed that the proposed controller is effectively working under PS condition.

5 Conclusion
The series connected boost derived micro converter configuration has been developed for MPPT operation of solar PV system under PS conditions supplying DC microgrid. This has been performed with modified P & O algorithm with a reduced number of sensors compared to that of the conventional DMPPT operation. The complete system has been developed using MATLAB/Simlink tool box and dSPACE(rti 1103) real time controller. The effectiveness of the DMPPT operation has been validated through different conditions such as step change in irradiation and degradation of the PV panels. Steady state and dynamic results obtained under various operating conditions show that the proposed control algorithm with the reduced number of sensors is effective in tracking the maximum power of PV panels in series configurations.

Nomenclature
MPP: Maximum Power Point
MPPT: Maximum Power Point Tracking
DMPPT: Distributed Maximum Power Point Tracking
GMPPT: Global Maximum Power Point Tracking
FPDC: Full Power DC-DC Converter
CPDC: Compensation Power DC-DC converter
DSO: Digital Storage Oscilloscope
P & O: Perturb and Observe
PS: Partial Shading
$D_i$: Duty ratio of $i^{th}$ converter
$i_{PVi}$: Instantaneous current of $i^{th}$ panel
$i_o$: Instantaneous output current
$v_{PVi}$: Instantaneous voltage of $i^{th}$ panel
$p_{PVi}$: Instantaneous panels power
$p_o$: Instantaneous output (DC microgrid) power
$p_{i}$: Converter losses
$R_s$, $R_sh$: Series and shunt resistance of PV panel
where $i = 1, 2, \ldots, N$ (N number of converters)
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Appendix A
The IGBT and diode power loss calculation is attained by the equations given in [31, 32].

The total power loss in IGBT is the sum of the conduction and switching losses, where, the conduction loss of IGBT

$$P_{\text{cond}} = V_{\text{on}} \left( \frac{i_o}{1-D} \right) + R_{\text{on}} D \left( \frac{i_o}{1-D} \right)^2.$$  \hspace{1cm} (18)

Switching loss of IGBT is

$$P_{\text{sw}} = (E_{\text{on}} + E_{\text{off}}) f_{\text{sw}}.$$ \hspace{1cm} (19)

In this experimentation, the boost converter is fabricated with an IGBT (IRGT1090U06) and diode (IXYS DSEI30-06A). The parameters of both the devices are

- $v_{\text{on}} = 2.0 \text{ V}$ for 30 A, $R_{\text{on}} = 33.33 \text{ mW}$, $t_f = 250 \text{ ns}$, $E_{\text{on}} = E_{\text{off}} = 0.05 \text{ mJ/A}$, and $f_{\text{sw}} = 10 \text{ kHz}$ for IGBT and
- $v_{\text{D(on)}} = 1.01 \text{ V}$, $R_{\text{D(on)}} = 7.1 \text{ mW}$, $v_{\text{fr}} = 7 \text{ V}$, and $t_{\text{fr}} = 350 \text{ ns}$ for diode.

The conduction loss of diode is

$$P_{\text{Dcond}} = v_{\text{D(on)}} i_o + R_{\text{D(on)}} i_o^2.$$ \hspace{1cm} (20)

The switching loss of the diode is

$$P_{\text{Dsw}} = (E_{\text{D(on)}} + E_{\text{D(off)}}) f_{\text{sw}}.$$ \hspace{1cm} (21)

The off-state energy losses are normally neglected [32]. The on-state energy loss is

$$E_{\text{D(on)}} = \frac{1}{2} i_o v_{\text{fr}} I_{\text{on}}.$$ \hspace{1cm} (22)

where $t_f$ and $v_{\text{fr}}$ are the turn-on recovery time and over-voltage and the procedure for calculating these values are given in [32]. The power loss due to the inductive resistance of the filter is

$$P_{\text{Dind}} = R_{\text{ind}} \left( \frac{i_o}{1-D} \right)^2.$$ \hspace{1cm} (23)

Hence, the total converter loss is

$$P_{\text{t}} = P_{\text{cond}} + P_{\text{sw}} + P_{\text{D(on)}} + P_{\text{Dsw}}.$$ \hspace{1cm} (24)