Knowlege Graph Embedding by Flexible Translation

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Abstract

Knowledge graph embedding refers to projecting entities and relations in knowledge graph into continuous vector spaces. State-of-the-art methods, such as TransE, TransH, and TransR build embeddings by treating relation as translation from head entity to tail entity. However, previous models can not deal with reflexive/one-to-many/many-to-one/many-to-many relations properly, or lack of scalability and efficiency. Thus, we propose a novel method, flexible translation, named TransF, to address the above issues. TransF regards relation as translation between head entity vector and tail entity vector with flexible magnitude. To evaluate the proposed model, we conduct link prediction and triple classification on benchmark datasets. Experimental results show that our method remarkably improve the performance compared with several state-of-the-art baselines.

1 Introduction

Knowledge graphs such as Wordnet [Miller, 1995] and Freebase [Bollacker et al., 2008] are useful resources for natural language understanding, question answering, web search, etc. A knowledge graph contains highly-structured and well-organized data, and is usually represented by directed graph in which nodes correspond to entities and edges correspond to relation, or simply by a set of triples (head entity, relation, tail entity) ((h, r, t) for short). Although there have been substantial achievements in building large-scale knowledge graph, the general paradigm to support computing is not clear. Indeed, traditional knowledge graphs are symbolic and logical frameworks which are not flexible enough to be fruitfully exported, especially to statistical learning approaches which require the knowledge to be computable in numerical forms.

Recently, knowledge graph embedding, which projects entity or/and relation into continuous vector spaces, has been a new proposal to offer the powerful capability of computing on knowledge graph. In this paradigm, the embedding representation of a single entity/relation encodes the global information of the entire knowledge graph, since it is obtained by minimizing a global loss function involving all entities and relations. Furthermore, the embedding representations are beneficial to a variety of applications such as question answering and web search concerning knowledge computation. Taking knowledge graph completion as an example, we can simply judge the correctness of a triple (h, r, t) by checking the compatibility of the embedding vectors of h, r and t.

A variety of approaches have been explored for knowledge graph embedding, such as neural network based [Bordes et al., 2011; Socher et al., 2013], and translation based [Bordes et al., 2013] approaches. Some notable works, including TransE [Bordes et al., 2013], TransH [Wang et al., 2014], and TransR [Lin et al., 2015] are simple, efficient, and effective.

Inspired by [Mikolov et al., 2013], TransE learns vector embedding for both entities and relations. In TransE, relation is represented as translation from head entity to tail entity in the embedding space, which applies h + r ≈ t, if (h, r, t) holds. However, TransE does not work well when dealing with relations of reflexive/one-to-many/many-to-one/many-to-many. Taking a one-to-many relation publish_song as the example, we have triples such as (Michael_Jackson, publish_song, Beat_It), (Michael_Jackson, publish_song, Billie_Jean) and (Michael_Jackson, publish_song, Thriller). As shown in Figure 1[a], considering the ideal embedding where h + r = t, the entities Beat_It, Billie_Jean and Thriller will get the same embedding vectors. Although TransE does not enforce h + r = t for golden triples during training, the tendency still exists.

As a variant of TransE, TransR models entities and relations in separate spaces and performs translation in the cor-
2 Related Work

There are a variety of models for knowledge graph embedding. Each model projects entities and relations into a continuous vector space and the triples are assigned with scores to represent their correctness. Two lines of works are surveyed here.

2.1 Translation-based Models

TransE \cite{Bordes2013TranslatingEM} represents relationships by translation vectors in an embedding space. It assumes that if \((h, r, t)\) holds, the embedding of the tail entity \(t\) should be close to that of the head entity \(h\) plus the relation vector \(r\), i.e., \(h + r \approx t\). Hence, TransE adopts \(f_r(h, t) = \|h + r - t\|_{1/2}\) as the score which is low when the triple is correct and high otherwise. TransE is very efficient and performs well to one-to-one relations whilst bad in dealing with reflexive /one-to-many/many-to-one/many-to-many relations.

TransH \cite{Wang2014KnowledgeGR} attempts to alleviate the problems of TransE when dealing with reflexive /one-to-many/many-to-one/many-to-many relations by modeling a relation as a relation-specific hyperplane with \(w_r\) as the normal vector together with a translation operation \(d_r\) on it. After projecting entity embeddings \(h\) and \(t\) to the hyperplane, on the same assumption as in TransE, the projections \(h_{\perp}\) and \(t_{\perp}\) are connected by \(d_r\) in a new space. Thus, TransH defines a scoring function \(f_r(h, t) = \|h_{\perp} + d_r - t_{\perp}\|^2\) to measure the plausibility that the triple is incorrect.

TransR \cite{Lin2015TranslationBasedMO} addresses the issue that some entities are similar in the entity space but comparably different in other specific aspects. The model builds embeddings in distinct entity space and multiple relation spaces and performs translation in the relation space. In TransR, each relation \(r\) is associated with a mapping matrix \(M_r\). Entities may be projected from the entity space to the relation space as \(h_r\) and \(t_r\). Similar to TransE, the score function is correspondingly defined as \(f_r(h, t) = \|h_r + r - t_r\|^2\) which produces lower scores for golden triples.

As mentioned, TransE, TransH, and TransR are all based on the score function \(f_r(h, t) = \|h + r - t\|_{1/2}\) of TransE. However, TransE ignores the relation categories and does not work well in dealing with one-to-many/many-to-one/many-to-many relations. Although TransH is capable of fixing the flaw, it introduces additional parameters, which sacrifices the efficiency of the model. For the TransR model, it still have the same problem as TransE.

2.2 Other Related Models

Besides TransE, TransH and TransR, there are many other models proposed for knowledge graph embedding. We introduce several typical models.
It cannot distinguish different relations. Structured Embedding introduces two independent projections for the entities in a relation. The basic idea is that when two entities belong to the same triple, their embedding should be close to each other in some subspace. The score function two entities belong to the same triple, their embedding should be close to each other in some subspace. The score function of the naive case of TransE, which sets all translation $r = 0$, i.e., the score function becomes $f_r(h, t) = \|h - t\|_{l_1/2}$. Obviously, it cannot distinguish different relations. Structured Embedding introduces two independent projections for the entities in a relation. The basic idea is that when two entities belong to the same triple, their embedding should be close to each other in some subspace. The score function for the triple is defined as $f_r(h, t) = \|W_{r,h} - W_{r,t}\|_1$. As pointed out by [Socher et al., 2013], this model is weak to capture the correlations between entities and relations because of the introduction of two separate matrices. Semantic Matching Energy [Bordes et al., 2014] captures the interactions of relation vectors and entity vectors through multiple matrix Hadamard products. Accordingly, the score function is the following linear form $f_r(h, t) = (W_{h,r} + b_1)^\top(W_{r,h} + W_{r,t} + b_2)$ or the bilinear form $f_r(h, t) = (W_{h,r} + b_1)^\top(W_{r,h} + b_2)$. Parameters are shared by all relations. Neural Tensor Network [Socher et al., 2013] defines an expressive score function as $f_r(h, t) = u_r^\top g(h^\top M_t + M_{t,h} + M_{r,t} + b_r)$ where $u_r$ is a relation-specific linear layer, $g()$ is the tanh operation. Even when the tensor $W_r$ degenerates to a matrix, it covers most other models. However the model complexity is much higher, making it difficult to handle large scale graphs.

We also treat Single Layer Model [Socher et al., 2013], Latent Factor Model [Jenatton et al., 2012] and RESCAL [Nickel et al., 2011] Nickel et al., 2012] as our baseline in experiments.

### 3 Method

To address the issues of TransE, TransH, and TransR as mentioned before, we propose a knowledge graph embedding model based on flexible translation (TransF). TransF can essentially overcome the problems of TransE in modeling reflexive/one-to-many/many-to-one/many-to-many relations. The details of the model are described in Section 3.1 Following the same principle of flexible translation, we also propose TransRF model which is an improved variant of TransR, as presented in Section 3.2.

Let's introduce some notations. $S$ denotes a set of golden triples, while $S'$ denotes a set of corrupted triples. A triple $(h, r, t)$ consists of two entities $h, t \in E$ (the set of entities) and relation $r \in R$ (the set of relations). We use the bold letters $h, r$ and $t$ to denote the corresponding embedding representations.

#### 3.1 Flexible Translation: TransF

We first analyze the limitations of TransE, TransR and TransH models. Then we explain our TransF model in detail.

As mentioned before, TransE and TransR work well to irreflexive and one-to-one relations but they have problems with reflexive/one-to-many/many-to-one/many-to-many relations. The reason is that both TransE and TransR adopt the score function $\|h + r - t\|_{l_1/2}$. When triple $(h, r, t)$ holds, the score function is low, meaning that $h + r \approx t$. More specifically, if with the ideal embedding using the function $h + r = t$ when $(h, r, t)$ holds, we can obtain: 1) if $(h, r, t)$ and $(t, r, h)$ are both correct, $r$ is a reflexive relation and $r = 0$, $h = t$; 2) if a set of triples $(h, r, t_i), \forall i \in 0, \cdots, n$ hold, $r$ is a one-to-many relation and $t_0 = \cdots = t_n$; 3) if a set of triples $(h_i, r, t), \forall i \in 0, \cdots, n$ hold, $r$ is a many-to-one relation and $t_0 = \cdots = b_n$. Although TransH can solve this problem, it introduces extra parameters for each relation and are not flexible and efficient enough to improve the TransR model.

To alleviate the problem of TransE and maintain the high efficiency, we apply $h + r \approx \alpha t$, $\alpha > 0$, instead of $h + r \approx t$, when $(h, r, t)$ holds. That means we only need to maintain the directions of vectors $h + r$ and $t$, but ignore their magnitudes. Therefore, 1) when $r$ is a reflexive relation, we get $h = \frac{1}{\alpha} r$, $t = \frac{1}{\alpha} r$, where $h + r \approx \alpha r$, $t + r \approx \alpha h$. 2) if $r$ is a one-to-many relation, we get $t_0 = \alpha t$, $\cdots$, $t_n = \frac{h + r}{\alpha}$; 3) if $r$ is a many-to-one relation, we get $t_0 = \alpha t - r$, $\cdots$, $t_n = \alpha t - r$. The score function is then defined as follows:

$$f_r(h, t) = (h + r)\top t$$

However, with the score function, the constraints on head entity $(h)$ and tail entity $(t)$ are unbalanced. More specifically, under the constraints, the range of $h$ is a line, and the range of $t$ is a plane. Considering the perfect no-error embedding, we discuss the constraints on tail entity and head entity separately. As shown in Figure 2(a), when the embedding vectors $h$ and $r$ hold, the range of the no-error embedding vector $t$ is a vector with the right arrow on the dotted line. However, as shown in Figure 2(b), when the embedding vectors $r$ and $t$ are known, the range of the perfect embedding vector $h$ is a vector with the starting point on the dotted line $a$ and the ending point on the dotted line $b$.

Since head entity and tail entity need to have the same effect during training, the constraints on them should be balanced. To this end, we design a Flexible Translation(TransF) model to address the unbalanced constraint problem. We modify the score function as follows:

$$f_r(h, t) = (h + r)\top t - h\top (t - r)$$

The score is expected to be higher for a golden triple while lower for a corrupted one. As shown in Figure 3, both TransF and TransE are presented the score distribution on benchmark datasets. It is clear that our TransF model discriminates the golden triples and corrupted triples much better than TransE.
functions. The objective is to ensure that a triple

In the golden set should have a higher score than a triple

We can improve the TransE related models to TransF re-

3.2 Enhancement of TransR: TransRF

We can improve the TransE related models to TransF re-

Accordingly, we can define the score function as

where \( h_r = hM_r \) and \( t_r = tM_r \). For each relation \( r \), \( M_r \) is the projection matrix which projects entities from the entity space to the relation space. We follow the constraints on the norms of the embeddings of \( h, r, t \) and \( \sum tM_r \) is a golden triple, TransRF adopts

\[ f_r(h, t) = (h_r + r)\top t_r + h\top_r (t_r - r) \quad (3) \]

3.3 Training Objective

All models are trained with contrastive max-margin objective functions. The objective is to ensure that a triple \((h, r, t) \in S\) in the golden set should have a higher score than a triple \((h', r, t') \in S'\) in the corrupted triple set, as follows:

\[ L = \sum_{(h, r, t) \in S} \sum_{(h', r', t') \in S'} \max(0, \gamma - f_r(h, t) + f_r(h', t')) \quad (4) \]

where \( \gamma > 0 \) is a margin hyperparameter. \( S \) is the training set of golden triples. \( S' \) is the set of corrupted triples. The corrupted triples are generated from the training triples with either the head or tail entity replaced by a random entity (but not both at the same time).

We adopt the mini-batched stochastic gradient descent (SGD) to optimize the objective function. The additional constraints on the norms of embedding parameters are explained with the model descriptions. For TransF, all embeddings are randomly initialized with a similar process of [Glorot and Bengio, 2010]. For TransRF, the initialization process is the same as TransR, and the projection matrices are initialized as identity matrix.

4 Experiments

In this section, we conduct extensive experiments to justify the proposed models. First, we evaluate our models on link prediction [Bordes et al., 2013] and triple classification [Socher et al., 2013] respectively. Second, to explain the remarkable improvements, we assess how well the models can discriminate the golden triples and corrupted triples with the score function, comparing with TransE.

Three benchmark datasets are adopted in the experiments: WN18 [Bordes et al., 2013] which is extracted from Wordnet [Miller, 1995]; and two dense subgraphs of Freebase [Bollacker et al., 2008], FB15K [Bordes et al., 2013] and FB13 [Socher et al., 2013]. Table I shows the statistics of these data sets.

### 4.1 Link Prediction

As reported in [Bordes et al., 2011, Bordes et al., 2013], link prediction is to predict the missing \( h \) or \( t \) given \( (h, r) \) or \( (r, t) \) respectively. In this task, we conduct the evaluation by ranking the set of candidate entities in knowledge graph, instead of offering a best matching entity. This experiment is conducted on two datasets, WN18 and FB15K.

**Evaluation protocol.** Following the protocol in TransE [Bordes et al., 2013], for each test triple \((h, r, t)\), we replace the head entity \( h \) by every entity in the knowledge graph, and rank these corrupted triples in descending order by the similarity score which is given by \( f_r \). Similarly, we repeat this procedure by replacing the tail entity \( t \). After collecting all these triples, we use two evaluation metrics: the mean rank of the correct entities (denotes as Mean Rank); the proportion of correct entity ranks within 10 (denotes as Hits@10).

We expect lower Mean Rank and higher Hits@10 for a better predictor. However, some corrupted triples should be considered as correct ones, since they actually exist in knowledge graph. Ranking such triples ahead of the original correct one should not be counted as an error. To eliminate such cases, we filter out those corrupted triples which appear either in the training, validation or test datasets. We term the former evaluation setting as "Raw" and the latter as "Filter".

**Implementation.** By sharing the same data sets, we directly refer to the baselines and experimental results reported in [Lin et al., 2015]. We select learning rate \( \lambda \) for SGD among \( \{0.0001, 0.001, 0.0035, 0.01\} \), the margin \( \gamma \) among \( \{0.25, 0.45, 0.6, 0.9\} \), the embedding dimension \( k \) among \( \{20, 50, 100, 200\} \) and batch size \( B \) among \( \{120, 480, 960, 1440\} \). In training TransF, the best configurations are \( \lambda = 0.01, \gamma = 0.9, k = 50, B = 960 \) on WN18; \( \lambda = 0.0035, \gamma = 0.45, k = 100, B = 960 \) on FB15K. For experiments with TransRF, the optimal configurations are: \( \lambda = 0.0001, \gamma = 0.25, k = 50, B = 960 \) on WN18; \( \lambda = 0.001, \gamma = 0.25, k = 50, B = 1440 \) on FB15K. For all the datasets, we scan all the training triples for 1000 rounds for training TransF and 500 rounds for training TransRF.

**Experiment Results.** Table II lists the results on WN18 and FB15K. It demonstrates that TransF, which take relation categories into consideration, outperforms TransE and other baselines on WN18 and FB15K. Furthermore, our TransF model, which is more efficient with less parameters, obtains comparable results to TransH. Comparing the TransR to the TransRF model, TransRF is consistently outperforming TransR on WN18 and FB15K. The reason why our models fail on Mean Rank on WN18 may be due to the small number of relations in the WN18 dataset. For a fair comparison, the reason why we first compare the results of TransE,
Table 2: Experiment Result on link prediction

| Data Sets | WN18 | FB15K |
|-----------|------|-------|
|           | Mean Rank | Hits@10(%) | Mean Rank | Hits@10(%) |
|           | Raw Filter | Raw Filter | Raw Filter | Raw Filter |
| Unstructured [Bordes et al., 2014] | 315 | 304 | 35.3 | 38.2 | 1,074 | 979 | 4.3 | 6.3 |
| RESCAL [Nickel et al., 2011] | 1,180 | 1,163 | 37.2 | 52.8 | 828 | 683 | 28.4 | 44.1 |
| SE [Bordes et al., 2014] | 1,011 | 985 | 68.5 | 80.5 | 273 | 162 | 28.8 | 39.8 |
| SME(linear) [Bordes et al., 2014] | 545 | 533 | 65.1 | 74.1 | 274 | 154 | 30.7 | 40.8 |
| SME(bilinear) [Bordes et al., 2014] | 526 | 509 | 54.7 | 61.3 | 284 | 158 | 31.3 | 41.3 |
| LFM [Jenatton et al., 2012] | 469 | 456 | 71.4 | 81.6 | 283 | 164 | 26.0 | 33.1 |
| TransE [Bordes et al., 2013] | 263 | 251 | 75.4 | 89.2 | 243 | 125 | 34.9 | 47.1 |
| TransH [Wang et al., 2014] | 318 | 303 | 75.4 | 86.7 | 211 | 84 | 42.5 | 58.5 |
| TransF | 403 | 390 | 76.0 | 90.2 | 220 | 89 | 40.5 | 61.2 |
| TransR [Lin et al., 2015] | 232 | 219 | 78.3 | 91.7 | 226 | 78 | 43.8 | 65.5 |
| TransRF | 343 | 342 | 95.2 | 95.3 | 54 | 49 | 72.7 | 73.5 |

Table 3: Detailed results on FB15K in terms of different relation categories, (%)

| Tasks | Predicting Head(Hits@10) | Predicting Tail(Hits@10) |
|-------|--------------------------|--------------------------|
| Relation Category | 1-to-1 | 1-to-N | N-to-1 | N-to-N | 1-to-1 | 1-to-N | N-to-1 | N-to-N |
| Unstructured [Bordes et al., 2014] | 34.5 | 2.5 | 6.1 | 6.6 | 34.3 | 4.2 | 1.9 | 6.6 |
| SE [Bordes et al., 2014] | 35.6 | 62.6 | 17.2 | 37.5 | 34.9 | 14.6 | 68.3 | 41.3 |
| SME(linear) [Bordes et al., 2014] | 35.1 | 53.7 | 19.0 | 40.3 | 32.7 | 14.9 | 61.6 | 43.3 |
| SME(bilinear) [Bordes et al., 2014] | 30.9 | 69.6 | 19.9 | 38.6 | 28.2 | 13.1 | 76.0 | 41.8 |
| TransE [Bordes et al., 2013] | 43.7 | 65.7 | 18.2 | 47.2 | 43.7 | 19.7 | 66.7 | 50.0 |
| TransH [Wang et al., 2014] | 66.7 | 81.7 | 30.2 | 57.4 | 63.7 | 30.1 | 83.2 | 60.8 |
| TransF | 74.2 | 65.6 | 50.4 | 60.5 | 74.9 | 59.8 | 60.4 | 63.4 |
| TransR [Lin et al., 2015] | 76.9 | 77.9 | 38.1 | 66.9 | 76.2 | 38.4 | 76.2 | 69.1 |
| TransRF | 74.3 | 66.8 | 50.5 | 76.6 | 75.4 | 55.9 | 67.1 | 79.0 |

TransH, and our TransF model then analyze the results between TransR and our proposed TransRF, is that TransR builds multiple relation spaces instead of one embedding space.

We dig into detailed prediction results with different types of relations including one-to-one/one-to-many/many-to-one/many-to-many relations, since TransF aims to handle these relation categories which TransE cannot. We classify the relations by following the same rules in [Bordes et al., 2013]. Then, we obtain 24% one-to-one relations, 23% one-to-many relations, 29% many-to-one relations and 24% many-to-many relations within 1,345 relations on the FB15K dataset. As shown in Table 3, TransF model consistently outperforms the TransE model. Meanwhile, TransF outperforms TransH in one-to-one/many-to-many relations for predicting tail and one-to-one/many-to-many relations for predicting tail. TransRF also outperforms TransR in dealing with many-to-one/many-to-many relations for predicting head and one-to-many/many-to-many relations for predicting tail. Specifically, TransF and TransRF models bring promising improvements on many-to-many relations, and additionally, the performance on one-to-one is also significantly improved, compared with TransE and TransH. This may be due to the fact that our TransF model also relaxes the geometric assumption of TransE.

Model Complexity Analysis. To analyze the efficiency of our model, we compare the theoretical number of parameters of the baselines and record the running time of TransF, TransRF and other baseline models for each training epoch. As demonstrated in Table 4, our TransF model keeps the same number of parameters as the TransE model, and TransRF also keeps the same number of parameters as TransR. However, TransH needs more parameters than TransF. Furthermore, the training time of TransH is nearly 24 times of that of TransE and TransF. The training time of TransRF is nearly the same as TransR. Therefore, our models are able to improve the knowledge graph embedding without sacrificing the efficiency.

4.2 Triple Classification

Following the experiment in [Bordes et al., 2013, Wang et al., 2014, Lin et al., 2015], we also evaluate our model on triple classification. Triple classification is a binary classification task which predict whether a given triple (h, r, t) is correct or not. This task is applied for answering question such as “Does Michael Jackson publish the song Beat it?”.
sets in this task: WN11 and FB13 released in NTN [Socher et al., 2013]; FB15K used in TransR [Lin et al., 2015].

Evaluation protocol. Following the protocol in NTN [Socher et al., 2013], we set a relation-specific threshold $T_r$ for prediction and then, for a triple $(h, r, t)$, if the similarity score obtained by $f$, is above $T_r$, the triple $(h, r, t)$ is predicted as positive, otherwise negative. The relation-specific threshold $T_r$ is determined by maximizing the classification accuracy on a validation set.

Implementation. We compare our models with the baseline methods reported in [Lin et al., 2015] for WN11, FB13 and FB15K. We enumerate learning rate $\lambda$ for SGD among $\{0.0001, 0.001, 0.002, 0.01\}$, the margin $\gamma$ among $\{0.1, 0.5, 1, 2, 2.25, 2.5\}$, the embedding dimension $k$ among $\{20, 50, 100\}$ and the batch size $B$ among $\{120, 480, 960, 1440\}$. For training TransF, the optimal configuration are: $\lambda = 0.01, \gamma = 2.25, k = 100, B = 960$ on WN11; $\lambda = 0.005, \gamma = 2, k = 100, B = 960$ on FB13; $\lambda = 0.002, \gamma = 0.5, k = 100, B = 960$ on FB15K. For experiments with TransRF, the best configurations are: $\lambda = 0.0001, \gamma = 2.5, k = 50, B = 960$ on WN11; $\lambda = 0.001, \gamma = 2.5, k = 50, B = 960$ on FB13; $\lambda = 0.001, \gamma = 0.1, d = 50, B = 120$ on FB15K. The number of training epochs is limited to 1,000 for TransF and 500 for TransRF.

Experiment Result. Evaluation results are reported in Table 5. It demonstrates that our TransF model outperforms all the baseline models significantly including TransE, TransH, and even TransR on WN11 and FB15K. On FB13, TransF beats all baseline models except the NTN model. As described in [Wang et al., 2014, Lin et al., 2015], FB13 is much denser than WN11 and FB15K where strong correlations exist between entities, and NTN can achieve better results by learning complicated correlations using tensor transformation from dense graph of FB13. Comparing TransRF and TransR, our TransRF model has higher accuracy than TransR on all datasets, especially on FB13 and FB15K.

4.3 Score Distribution

To explain the remarkable improvements obtained by our model on these tasks, we assess whether our model can better distinguish the positive and negative triples, compared with TransE. For embedding vectors, we directly use the embedding results which are trained for the link prediction task on WN18 and FB15K. Then, two triple sets of positive and negative are built for comparison, where the positive triples are the ones in the test dataset. The negative triple set is constructed in three ways: replacing the head entity randomly from each of the positive triple; replacing the tail entity randomly; and randomly selecting two entities and a relation to assemble a new triple. The triples generated by the first two methods is called semi-negative triples and those by the third method negative ones. While generating negative triples, we guarantee the them do not exist in the knowledge graph.

As shown in Figure 3, the TransF model distinguishes positive and negative triples remarkably better than TransE. In the TransF model, the boundary of scores for positive and negative triples is clear on both WN18 and FB15K datasets, as depicted in Figure 3(b)(d). In comparison, in the TransE model, we cannot find a clear boundary of scores on both WN18 and FB15K datasets, as can be seen from Figure 3(a)(c). For the TransF model, the score of positive triple is expected to be higher than that of negative triple. For the TransE model, the score of positive triple is expected to be lower than that of negative triple.

5 Conclusion

In this paper, we propose knowledge embedding models with flexible translation, which are effective, efficient and portable. The idea of flexible translation is to ensure that the sum vector of a head entity vector and a relation vector has the same direction with a tail entity vector but with flexible magnitude. The proposed models, TransF and TransRF, not only well address some existing issues in previous models when dealing with reflexive/one-to-many/many-to-one/many-to-many relations, but also maintain low complexity and high efficiency. We conduct extensive experiments on benchmark datasets for the tasks of link prediction and triple classification, and results show that our TransF and TransRF models obtain substantial improvements over baselines.

| DataSets | WN11  | FB13  | FB15K |
|----------|-------|-------|-------|
| SE [Bordes et al., 2011] | 53.0  | 75.2  | -     |
| SME (bilinear) [Bordes et al., 2014] | 70.0  | 63.7  | -     |
| SLM [Socher et al., 2013] | 69.9  | 85.3  | -     |
| LFM [Jentall et al., 2012] | 73.8  | 84.3  | -     |
| NTN [Socher et al., 2013] | 70.4  | 87.1  | 68.5  |
| TransE [Bordes et al., 2013] | 75.9  | 70.9  | 79.6  |
| TransH [Wang et al., 2014] | 77.7  | 76.5  | 79.0  |
| TransR [Lin et al., 2015] | 85.5  | 74.7  | 81.7  |
| TransF | 86.6  | 82.9  | 88.8  |
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