Oscillations of the superconducting critical current in Nb-Cu-Ni-Cu-Nb junctions

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We report on experimental studies of superconductor-ferromagnet layered structures. Strong oscillations of the critical supercurrent were observed with the thickness variation of the ferromagnet. Using known microscopic parameters of Ni, we found reasonable agreement between the period of oscillations and the decay of the measured critical current, and theoretical calculations.

The interplay between superconductivity and ferromagnetism is an old subject which was studied extensively over decades. The most striking effect in such systems is the formation of the so-called \( \pi \) phase junction in a superconductor-ferromagnet-superconductor (SFS) structure. One of the manifestations of the \( \pi \) phase is a non-monotonic variation of the critical temperature \( T_c \) with the variation of the ferromagnetic layer thickness, \( d \). Oscillatory dependence of \( T_c \) vs. \( d \) of SF multilayers has been observed by few groups; however, other groups reported monotonic behavior in similar structures. Interpretations of these experiments suggested the \( \pi \) junction mechanism as well as some other origins of the effect. The recent observation of non-monotonic behavior of the critical current as a function of temperature in weak-ferromagnetic layer of \( \mathrm{Cu}_x\mathrm{Ni}_{1-x} \) between two Nb layers is considered as an unambiguous proof of the \( \pi \) phase formation. Another interesting theoretical prediction concerns non-monotonic behavior of the critical current as a function of the thickness of the ferromagnetic layer \( d \). According to the above predictions, the critical current \( I_c \) is expected to oscillate and decay as \( d \) is increased. To the best of our knowledge, such a behavior has not been reported so far.

In this paper, we present the experimental evidence of oscillatory behavior of the critical current vs. thickness variation of ferromagnetic Ni layer. We also show a reasonable agreement between our data and the theories in the appropriate limit of \( E_{cz} \gg \hbar/\tau \gg k_B T_c \). Here, \( \tau \) and \( E_{cz} \) are the electron relaxation time and the exchange energy of the ferromagnet, and \( T_c \) is the critical temperature of the superconductor.

We have studied temperature and thickness dependence of the critical current in Nb-Cu-Ni-Cu-Nb junctions. Additionally, we have studied the thickness dependence of critical current of similar junctions without a Ni layer. The junctions with 10x10\( \mu \text{m}^2 \) area were fabricated with the standard photolithography technique. The process contained three stages of lithography: liftoff of the bottom Nb-Cu layer, liftoff of the variable thickness Ni or Cu layers, and liftoff of the top Cu-Nb layer.Nb films were sputtered using a magnetron gun and \textit{in situ} covered with the Cu layer by thermal evaporation, for preventing the Nb oxidation. The ferromagnet layers of Ni were e-gun evaporated in a separate vacuum chamber, and subsequently covered \textit{in situ} by Cu. It is important to emphasize that all samples were prepared simultaneously. The variation of Ni thickness for Nb-Cu-Ni-Cu-Nb junction and variation of Cu for Nb-Cu-Nb junctions was obtained by a specially designed shutter, which exposed the samples in sequence, so that every sample was exposed to the evaporating Ni or Cu for additional fragments of time. This method guaranteed that all the interfaces between each layer in our multilayer structure are identical, and the only difference between the samples is their Ni or Cu thickness. The thickness of each Nb layer was 2000Å. The total thickness of the Cu in the Nb-Cu-Ni-Cu-Nb junctions was 2400Å and the Ni thickness varied from 10A to 90Å.

In the other set of junctions, namely Nb-Cu-Nb, the Cu thickness varied from 500Å to 10000Å. The structure of these junctions is shown schematically in the inset of Fig. 1.

Typical resistance of both types of junctions was around 100\( \mu \Omega \), independent of both Ni and Cu thicknesses. The critical temperature of the Nb was about 8.5K. The measured resistivity of Ni layer \( \rho = 31 \mu \Omega cm \), together with the known value \( \rho_l = 1.5 \cdot 10^{-11} \Omega cm^2 \), allowed us to establish the mean free path \( l = 48\AA \).

![Image](https://example.com/fig1.png)

**FIG. 1.** \( dV/dI \) of one of the samples. The critical current was defined as the onset of the peak. In the inset: schematic picture of a Nb-Cu-Ni-Cu-Nb junction.

The measurements were performed in \( ^4 \)He cryostat in the range from 6.5K down to 1.5K. The critical current was measured by passing a DC current with a small AC modulation through the sample. The AC voltage which
appeared above the critical DC current was picked up by lock-in amplifier operated in a transformer mode.

A typical differential resistance of both types of junctions vs. DC current is plotted in Fig.1, which clearly indicates on the sharp onset of dissipation at $I = I_c$. First, we show results of the Nb-Cu-Nb set (Fig.2). As expected, the critical current $I_c$ normalized to the length of the junction $L$, decreases exponentially with $L$. From the decay of the critical current we found the thermal length of the Cu, $L_T = \sqrt{\hbar D/2\pi k_B T} = 1600\,\text{Å}$ at 4.2K, and the diffusion constant $D = 860 \, \text{cm}^2/\text{s}$.

![Fig. 2. The normalized critical current $I_c/L$ of a Nb-Cu-Nb junctions as a function of the Cu thickness $L$. The straight line represents the theoretical decay.](image)

Very different thickness dependence was found in the Nb-Cu-Ni-Cu-Nb junctions. Fig.3 shows the thickness dependence of the critical current in these junctions at $T = 4.2K$. In spite of the large error bars, the non-monotonic variation of the critical current is quite evident, namely, the deviations of the data from the exponential decay surmounts by far the uncertainty of each measured point.

A further, and even a stronger evidence for the oscillatory behavior is provided by temperature dependence of the critical current. Fig.4 shows a family of $I_c$ vs. $T$ curves for all Ni thicknesses, which are normalized to their values at 4.2K. We define the slope $\alpha_T$ of temperature variation, namely $\alpha_T \equiv (dn) (\ln I_c(T))/dT$, and plot these values as a function of $d$ in Fig.3 (squares). Oscillations of $\alpha_T$ are very prominent, and are in anti-phase with the oscillations of the critical current. Unlike the critical current, which had quite large experimental error bars, the slope of the temperature dependence had error bars of only few percents. Such a behavior of $\alpha_T$ as a function of $d$ is intimately related to the variation of the critical current oscillations amplitude with temperature. Although the amplitude of the oscillations decreases at high temperatures, their relative value increases, and on a semi-logarithmic plot of Fig.4 the oscillatory behavior of $I_c$ is more pronounced at higher temperatures.

![Fig. 3. Critical current of the Nb-Cu-Ni-Cu-Nb junctions as a function of the Ni layer’s thickness $d$ at 4.2K (circles). The dependence of the slope $\alpha_T$ on $d$ is represented by squares. Both the dashed and dotted lines are only for guiding the eye.](image)

![Fig. 4. Critical current as a function of temperature of the Nb-Cu-Ni-Cu-Nb junctions for different thicknesses of the Ni layer.](image)

We would like to start our discussion with what is well known for superconductor-normal-superconductor (SNS) junctions. The dependence of critical current of such junctions on the thickness of N layer is exponential, $I_c \propto e^{-L/L_T}$ for $L > L_T$. In the opposite limit, where $L < L_T$, $I_c$ approaches a constant value. This behavior has been observed in few experiments for different material systems, including our sample presented in Fig.2.
expected theoretically, and had never been observed experimentally in SNS structures. Since the thickness of Ni is the only parameter which is varied in our Nb-Cu-Ni-Cu-Nb samples, it is reasonable to assume that the oscillations observed in the data are due to the presence of Ni in the structure.

As mentioned in the introduction, oscillatory behavior of the critical current vs. the thickness of the ferromagnetic layer is predicted theoretically. The origin of these oscillations is the phase shift acquired by electron-hole Andreev particles upon entrance into the ferromagnet, due to their different spin orientations. Several expressions have been derived for the critical current in various limits of the strength of $E_{ex}$, thickness of the ferromagnet $d$ and disorder. Since in our experiment we have determined only the magnitude of the critical current $I_c$, the formulae below will be written for the absolute value $|I_c|$. For the clean, thin and strong ferromagnetic layers $l > \nu_f/E_{ex} d$, the critical current should vary with the thickness as:

$$I_c \sim |\sin(2E_{ex}d/\nu_f)|/(2E_{ex}d/\nu_f) \quad (1)$$

The dependence of absolute value of the critical current is shown on Fig. 5 by dashed line. In the opposite limit, namely $l < d$, the following dependence was derived (dotted line in Fig. 5):

$$I_c \sim y e^{-y/\nu_f} \sin(y + \pi/4) \quad y = \sqrt{hD/4E_{ex}} \quad (2)$$

Another expression for the critical current in the limit $l > \nu_f/E_{ex}$, is given by

$$I_c \sim \left| \text{Re} \sum_{\omega_n > 0} \frac{\Delta^2}{\Delta^2 + \omega_n^2} \int_{-1}^{1} \frac{\mu d \mu}{\sinh(k_{ex}d/\mu l)} \right| \quad (3)$$

where $\omega_n = \pi T k_B (2n + 1)$ is the Matsubara frequency, $n$ is an integer number, $k_{ex} = (1 + 2\omega_n \tau / \hbar) - 2iE_{ex}\tau / \hbar$, $\mu = \cos \theta$, $\theta$ is the angle between the momentum and the normal to the SF interface, and $\Delta$ is the order parameter in the superconductor. The solid line of Fig. 5 represents the above expression. In fitting our data to the expressions for all limits, we have used $\nu_f = 2.8 \times 10^9 m/sec$ and $L = 48A$ (based on the resistivity measurements of Ni). Therefore, the only fitting parameter apart from the numerical prefactor was the strength of the exchange interaction $E_{ex}$.

The periodicity of oscillations in Eq. (3) $L_{osc} \sim \pi \nu_f/E_{ex}$, $\simeq 54A$ fits the best our data when $E_{ex} = 107 \pm 3 meV$. Note, that $L_{osc}$ is twice larger than the periodicity observed in Fig. 5, due to the absolute value taken for $I_c$. In order to have similar periodicity in Eq. (3), we have used weaker exchange field $E_{ex} = 86 meV$. All values are close to the recently reported value $E_{ex} = 115 meV$.

![FIG. 5. Critical current as a function of the thickness of the Ni layer at different temperatures.](image1)

The curve given by Eq. (3) in Fig. 6 follows the decay and the phase of the oscillations of the measured $I_c$ closer than the other two curves for large $d$. Furthermore, we estimate $\nu_f/E_{ex} = 17A$ which is smaller than the measured mean free path $l = 48A$, and therefore, the validity of using Eq. (3) $l > \nu_f/E_{ex}$, is justified. However, since Eq. (3) is valid only for $d > l$, the data points should follow Eq. (3) for $d < 40A$. We thus conclude that our data is consistent with Eq. (3) and Eq. (1) in their appropriate limits. Therefore, we give the fit of Eq. (3) and Eq. (1) to our data for four temperatures in Fig. 7.

![FIG. 6. Critical current of the Nb-Cu-Ni-Cu-Nb junctions at 4.2K, and the theoretical fits. The dashed line represents Eq. 1, the dotted line Eq. 2, and the solid line Eq. 3.](image2)
FIG. 7. Critical current of the Nb-Cu-Ni-Cu-Nb junctions at 1.5K, 4.2K, 5.2K and 6.5K, and the theoretical fits according to Eq. 3 (solid line) and Eq. 1 (dashed line).

The oscillations of $\alpha_T$ (Fig. 3), which slightly smear the oscillations of $I_c$ (Fig. 5), are not accounted by any of the mentioned theories and have only a minor effect on the overall quality of the fit presented in Fig. 7. A possible origin of this effect could be related to the presence of normal metal on both sides of the ferromagnetic layer. The structure we have used contains layers of Cu of a combined thickness $L = 2400 \ \AA$, which is much larger than the thickness of the Ni layer. It is obvious that at high temperatures ($L_T < L$) the contribution of Andreev particles propagating via short diffusion path is predominant, since paths which are much longer than $L$ do not contribute to the supercurrent. At low temperatures, where $L_T > L$, the contribution of longer paths is not negligible. The latter implies that the impact of the trajectories crossing Ni layer several times is higher at low temperatures. The multiple crossing of the ferromagnetic layer could produce additional harmonics of the basic frequency of the oscillations, which will smear the non-monotonic behavior. This multiple crossing has not been considered in the existing theories for S-F-S junctions, and therefore might be responsible for the observed temperature dependence of the oscillations in S-N-F-N-S junctions (Fig. 3).

In summary, we have observed the oscillations and the decay of the critical current in Nb-Cu-Ni-Cu-Nb junctions upon the increase of the thickness of the Ni layer. We found a reasonable agreement with the recent theoretical calculations in the appropriate limit. The puzzling temperature dependence of the oscillations' amplitude remains unexplained.

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