Faint satellite population of the NGC-3175 Group – a Local Group analogue

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ABSTRACT

In this paper, we identify and study the properties of low-mass dwarf satellites of a nearby Local Group analogue – the NGC-3175 galaxy group with the goal of investigating the nature of the lowest mass galaxies and the ‘Missing Satellites’ problem. Deep imaging of nearby groups such as NGC-3175 is one of the only ways to probe these low-mass galaxies which are important for problems in cosmology, dark matter and galaxy formation. We discover 553 candidate dwarf galaxies in the group, the vast majority of which have never been studied before. We obtained R and B band imaging, with the European Southern Observatory 2.2 m, around the central ∼500 kpc region of NGC-3175, allowing us to detect galaxies down to ∼23 mag (MB ∼ −7.7 mag) in the B band. In the absence of spectroscopic information, dwarf members and likely background galaxies are separated using colour, morphology, and surface brightness criteria. We compare the observed size, surface brightness, and mass scaling relations to literature data. The luminosity function with a faint end slope of α = −1.31, is steeper than that observed in the Local Group. In comparison with simulations, we find that our observations are between a pure Λ cold dark matter model and one involving baryonic effects, removing the apparent problem of finding too few satellites as seen around the Milky Way.

Key words: galaxies: dwarf – galaxies: groups: individual: NGC 3175 – galaxies: luminosity function, mass function.

1 INTRODUCTION

The Λ cold dark matter (ΛCDM) model has enjoyed considerable success in explaining the observed properties of structure formation and growth. This model matches with the observed fluctuations in the cosmic microwave background power spectrum (Hinshaw et al. 2013; Planck Collaboration 2014), the growth of large scale structure, quasar absorption lines, and the Lyman α forest (Springel, Frenk & White 2006). Because of this, one main focus over the past two decades has been to constrain or modify ΛCDM by searching for deviations from observations at small scales, such as within galaxy groups.

In a hierarchical scenario, galaxies assemble via mergers of smaller dark matter (DM) haloes where the merging process is not entirely smooth, i.e. substructures (haloes) are not always destroyed. Numerical simulations of pure DM particles indeed predict thousands of DM haloes orbiting the Milky Way (MW) and the Local Group (LG) compared to the few tens and hundreds, respectively, of observed satellite galaxies (Kauffmann, White & Guiderdoni 1993; Klypin et al. 1999; Moore et al. 1999; Springel et al. 2008) – this is known as the ‘missing satellites problem’. In particular, it was found by Klypin et al. (1999) that the discrepancy in the abundance of satellites between the hierarchical models and observations occurs below v_{\text{circ}} ∼ 50 km s^{-1}, corresponding to the faint end of the luminosity function. The study of dwarf galaxy population is therefore an important probe of the hierarchical ΛCDM model at small scales.

Since it was first shown that substructure would likely survive in galactic haloes, there has been considerable effort towards trying to reconcile ΛCDM with observations. Theories have been focused on producing realistic MW halo simulations by invoking various baryonic physics including winds and, stellar and supernova feedback effects all of which, suppress star formation in low-mass galaxies (e.g. Scannapieco et al. 2009; Wadepuhl & Springel 2011; Scannapieco et al. 2012). In addition, feedback from active galactic nuclei...
(AGN) has also been suggested to suppress star formation, even in the most massive dwarf galaxies (Dashyan et al. 2018).

Although the most recent generation of cosmological simulations (e.g. EAGLE project: Schaye et al. 2015; Crain et al. 2015 and APOSTLE: Fattahi et al. 2016) benefit from the increase in computational power, higher resolution, and the incorporation of feedback effects, there remains a need to implement the uncertain subgrid physics. For example, Scannapieco et al. (2012) compare the formation of a MW analogue using 13 different cosmological simulation codes in a ΛCDM structure formation scenario. Each code is run with the same initial conditions, but the outputs exhibit large variations in stellar mass, size, morphology and gas content.

Observationally, the census of LG satellites has been largely complete at the bright end, and thus the focus over the past decade has shifted to detecting ever fainter satellites (MB complete at the bright end, and thus the focus over the past decade content. Simulation codes in a ΛCDM analogue. This group was chosen based on both the similarity of MW, where the differences between models and observations is the most massive dwarf galaxies (Dashyan et al. 2018).

To the LG. Our aim is to identify the satellite population, study their properties, and carry out an initial comparison with the predictions from ΛCDM structure formation scenario. Each code is run with the same initial conditions, but the outputs exhibit large variations in stellar mass, size, morphology and gas content.

In this study, we focus on the NGC-3175 group – a nearby LG analogue. This group was chosen based on both the similarity of the MW and the LG may not be representative of their mass scale. Additionally, observations have shown that the Magellanic Clouds may have a satellite system of their own (e.g. Koposov et al. (2015); Torrealba et al. (2018)) which has introduced debate on the membership of some newly discovered satellites to the LMC or the MW. Proper motions from Gaia data release 2 find some of the newly discovered dwarf galaxies to be inconsistent with being associated to the Magellanic Clouds (Kallivayalil et al. 2018). This ongoing debate in the literature suggests a need to study abundance and properties of satellites around analogues, beyond the LG.

In the nearby universe, studies of satellite properties of hosts with different masses to the MW have already begun (e.g. NGC 253: Sand et al. 2014; NGC 3109: Sand et al. 2015; NGC 6503: Koda et al. 2015; NGC 2403: Carlin et al. 2016; M101: Merritt, van Dokkum & Abraham 2014; Benneke et al. 2017; M81: Chiboucas et al. 2013; Centaurus A: Crnojević et al. 2016). A large survey is also being led to study the satellite population around 100 MW analogues - the SAGA survey (Geha et al. 2017). Initial results from SAGA analogues hosts find the existence of the missing satellites problem. However, this survey has a magnitude limit of M_R ~ -12.3, whereas many satellites fainter than this limit have been found around the MW, where the differences between models and observations is the most acute.

In this study, we focus on the NGC-3175 group – a nearby LG analogue. This group was chosen based on both the similarity of K-band luminosities of the two large galaxies to the LG, and the group’s local environment. The group consists of two large spiral galaxies, NGC-3137 (M_K = -22.2) and NGC-3175 (M_K = -22.9) (Skrutskie et al. 2006). In comparison, the M31 has M_K = -23.4, which is computed using m_K = 1.1 mag (Jarrett et al. 2003) and a distance of 784 kpc (Stunek & Garnavich 1998). The MW has M_K = -24.0 (Malhotra et al. 1996; Drimmel & Spergel 2001). In addition, the group also contains other low-mass spiral galaxies, comparable to the LG. Our aim is to identify the satellite population, study their properties, and carry out an initial comparison with the predictions from ΛCDM.

### Table 1. Properties of the imaging data of the seven fields covering the central regions of NGC-3175, acquired from the ESO WFI instrument.

| Field | Exposures (R,B) | Seeing FWHM (R,B) (arcsec) |
|-------|-----------------|---------------------------|
| F1    | 15, 17          | 1.14, 0.95                |
| F2    | 15, 10          | 0.97, 0.98                |
| F3    | 15, 15          | 1.12, 1.24                |
| F4    | 15*, 15         | 1.70, 1.43                |
| F5    | 14, 15          | 0.95, 1.06                |
| F6    | 15, 15          | 1.02, 0.94                |
| F7    | 3, 15           | 1.26, 0.98                |

This paper is organized as follows: Section 2 provides an overview of the imaging data from the European Southern Observatory (ESO) Wide-Field Imager (WFI) telescope. Section 3 describes the SExtractor configuration used for object detection and star–galaxy separation to generate a sample of potential dwarf candidates. Section 4 describes the implementation of GALFIT, using GALAPAGOS-2 to fit surface brightness (SB) profiles of the sample, and examines the model fitting quality through comparisons with simulated objects. We also determine here the criteria for defining group membership of the dwarf galaxy sample. We analyse the properties of the dwarf candidates, in comparison with observations from literature data in Section 5. The cosmological implications of our findings are explored in Section 6 by the way of comparisons to various ΛCDM simulations of the LG. We provide our conclusions in Section 7.

In this paper, we use a ΛCDM cosmology with Ω_m = 0.3, Ω_Λ = 0.7, and H_0 = 70 km s^{-1} Mpc^{-1}. We use a distance of 14 Mpc to NGC-3175 (Sorce et al. 2014) in order to compute absolute magnitudes of the dwarf candidates. The distance modulus uncertainty of 0.43 mag (Sorce et al. 2014) from the Tully–Fischer distance estimate corresponds to an 18 per cent uncertainty in the quoted distance. This does not affect our background selection, instead only shifts the range of the parameters that are derived in this paper based on the assumed distance, such as absolute magnitude, physical size, and luminosity/mass.

### 2 DESCRIPTION OF THE DATA

The imaging data used in this paper were obtained from the ESO WFI instrument, mounted at the Cassegrain focus on the 2.2 m Max Planck-ESO (MPG) telescope at the La Silla observatory, Chile (Baade et al. 1999). The WFI has a large field of view of 34 arcmin × 33 arcmin and a detector arrangement consisting of 4 × 2 mosaic of 2k × 4k CCDs with a pixel scale of 0.238 arcsec pixel^{-1}. Imaging data were acquired in the broadband R (λ_central/FWHM:651.725 nm/162.184 nm) and B (451.0 nm/133.5 nm) bands in visitor mode between 2011 Jan 30 and 2011 Feb 06. The images were taken in seven different fields to cover the central ~500 kpc of the NGC-3175 group. For each of the seven pointings, multiple dithered exposures (typically 15) with an exposure time of 400 s or 600 s each (see Table 1) were taken. This allows our imaging data to have total integration times of typically 9000 s (~2.5 h) and to be 95 per cent complete down to M_B ~ −8.
Figure 1. The first field, F1R, with a field of view of 36 arcmin × 34 arcmin showing NGC-3175 at the left corner.

As such, the properties of the combined image for each field vary and are summarized in Table 1. We show the R band field with the NGC-3175 in Fig. 1.

Prior to the analysis, the raw images were processed which included bias subtraction, flat field correction, and registration to produce the seven fields described in Table 1. Overscan and trim methods were utilized to remove readout bias, whilst dark frames taken during the observation period were used to remove thermal electron counts from each CCD in the WFI array. The registration was performed to a common WCS using the NASA/IPAC UNSO B1 catalogue (Monet et al. 2003).

3 GALAXY DETECTION AND STAR REMOVAL

Detection of objects in our images is done by Source Extractor (SExtractor; Bertin & Arnouts 1996). SExtractor is an algorithm that automatically detects, deblends and performs astrometry and photometry of objects, optimized for speed and large images. We use SExtractor in ‘dual band mode’, which allows us to specify a detection and a measurement image. The former image is used for detection and deblending purposes, while the latter is used for photometry. The R band is used as the detection image as it is the deepest image in every field, and photometry is done in both of the imaging bands. Such a method ensures that the same sized aperture is used to measure the magnitude in both bands, enabling an accurate measure of the colour.

To run SExtractor in dual mode, we require the R and B band images to be registered and aligned. We work in pixel coordinates, and compute the geometric transformation required to map the R band coordinates to that of B band by fitting a power series to the fifth order in x and y which accounts for x and y shifts, x and y scale factor and a rotation. We obtained accurate positions of the same set of stars that are non-saturated in both bands. Stars spanning the entire image are used to increase the accuracy of the alignment. To check alignment, we compute the centroids of the reference stars in both the R and B aligned images, finding that our best fields are aligned to within 0.01 arcsec and the worst to within 0.05 arcsec, corresponding to the image with the worst seeing, F4.

3.1 Object detection

Within an astronomical image the flux measured of a given pixel is the sum of the background (sky) intensity and the object’s intensity. As we aim to detect the faint dwarf galaxy population in our imaging data, we require good background estimation. In the following section, we describe in detail the choice of the main SExtractor parameters that affect the background determination and object detection. The first step of SExtractor is background measurement based on a method of $\kappa, \sigma$ clipping, where values that deviate more than $\pm3\sigma$ from the mean are removed and the mean (for non-crowded fields) or mode (for crowded fields) of the remaining pixels is used to estimate the background (Bertin & Arnouts 1996).

We choose the size of the background grid across which the background value is interpolated to be larger than the largest objects in the image. This ensures that small scale variations in the background are accounted for while not overestimating the background due to flux from objects.

After the background subtraction process, we use a Gaussian filter to smooth the image as this filter is found to be best for the detection of faint objects.
The next SExtractor step is the detection of objects using a simple threshold process. A detection threshold of 6σ above the background was found to be ideal at detecting all of our faint objects while maintaining the number of spurious detections to <2 per cent, which were later manually removed.

Accurate deblending of objects that appear nearby in sky projection is crucial for identifying sources to which the SB profile needs to be fit (Section 4). The default deblending parameters were found to work best with our data, as listed in Table 2. A summary of other main SExtractor configuration parameters used in this study are also outlined in Table 2.

After the background estimation and object detection process, photometry on both the imaging bands is carried out using SExtractor by measuring the flux within an aperture. To determine a galaxy’s total flux, we define the extent of a galaxy using the Kron radius, $R_1$ which defines the first moment of a galaxy as:

$$R_1(R) = \frac{2\pi \int_0^R I(x) x^2 dx}{2\pi \int_0^R I(x) x dx}$$

(1)

where $x$ is the radius. We use an aperture of size 2.5$R_1$ (defined using the $R$ band) to measure the flux of an object. Such a size has been shown to theoretically contain more than 90 per cent of an object flux for Sérsic indices ranging from 0.2 to 10 (Graham & Driver 2005). Magnitudes measured within this aperture are known as Kron magnitudes.

### 3.2 Star–galaxy separation

To identify stars, we use SExtractor’s neural network based star–galaxy separator, stellaricity index (CLASS_STAR). The stellaricity index can range from 0 for extended objects, to 1 for point-like sources and requires an estimate of the seeing and the pixel scale of the image to be computed. We calculate the seeing of our images by measuring the point spread function (PSF) from isolated non-saturated stars. The PSF is measured as the FWHM of the distribution of light within these stars. We take multiple measurements across each image and average them to get an estimate of the seeing for each particular image. The variation across each image in the PSF size is however negligible. We also use the stellaricity index from SExtractor to identify stars. This is a procedure in SExtractor which determines whether objects are extended or consistent with a point source.

Using a very high value of stellaricity index likely produces a high completeness of galaxies but also includes a large contamination of stars which would have to be manually removed, and vice versa. Furthermore, the robustness of the stellaricity index decreases dramatically at faint magnitudes (Bertin & Arnouts 1996; Chen et al. 2002) and, when the sizes of objects are less than or comparable to the FWHM of the PSF. For the removal of stars, we perform various stellaricity index cuts and visually inspect any misclassified stars or galaxies. Via this process, we find that using a stellarlicity index >0.8 provides a good compromise between achieving high completeness (see Section 4.2.1) and purity of objects classified as galaxies.

Fig. 2 shows a plot of the central 1 arcsec aperture magnitude against the Kron magnitude, where our chosen stellaricity index cut identifies a linear stellar locus with a bright end tail corresponding to saturated stars. All objects that lie within 4$\times$ 4 isophotal area of such saturated stars are then removed from further analysis due to contamination from saturation spikes, and reflection of the telescope field corrector.

We also remove objects with SExtractor $R_1$ < 1.4 arcsec (~95 parsec) as these objects are likely background or compact stellar systems [such as globular clusters and UCDS; Conselice, Gallagher & Wyse (2002); Norris et al. (2014); Gregg et al. (2009); Liu et al. (2015)]. This will miss out any compact dwarf galaxies; however, such objects are very rare and mostly found in rich clusters (Penny, Forbes & Conselice 2012).

Finally, the reduced catalogue obtained after the aforementioned star removal and size cut criteria for all our fields is visually inspected. In this process, we manually add back any missed galaxies without using any selection criteria based on size or structural/morphological features so as to avoid excluding possible interesting objects from further analysis. It is also found that usually <1.5 per cent of the objects in the reduced catalogue are stars misclassified as galaxies, however, this number rises to ~10 per cent for one of the fields.

The end result of repeating the first pass through SExtractor on all of our fields is a catalogue of 2574 potential dwarf candidates which are to be model fitted to calculate accurate shape parameters. As we show later, this number is ~5 times larger than the final catalogue of dwarf candidates, from which we can infer that the first pass through SExtractor is unlikely to have missed a significant fraction of dwarf candidates.

### 4 GALAXY MODEL FITTING

Photometry from SExtractor such as Kron magnitudes, calculated within the Kron aperture can miss some fraction of the flux of our objects, as mentioned in Section 3, affecting the estimation of shape and ellipse parameters of a galaxy. One must perform two-dimensional light profile fitting to determine accurate structural properties of galaxies. Many algorithms such as GIM2D (Simard et al. 2002) and BUDDA (de Souza, Gadotti & dos Anjos 2004) exist for this task, the most versatile and commonly used of which is GALFIT (Peng et al. 2002). GALFIT offers the ability of simultaneous fitting of multiple objects within the image and computes the best fitting model by a method of least squares minimization, where the goodness of the fit is determined by computing the
4.1 Automated fitting using GALAPAGOS-2

The task of manually fitting the 2754 objects identified in all of our fields, while adequately accounting for flux contribution due to nearby sources in a consistent method, is a very difficult task. We thus make use of GALAPAGOS-2 (Häußler et al. 2013), an IDL routine which automates the process of running SEXTRACTOR, cutting postage stamps for the potential dwarf candidates, performs sky estimation and performs multiband fitting using GALFIT-M (multiband version of GALFIT). For a full description of the functional blocks of GALAPAGOS-2, we refer the reader to the release paper (Häußler et al. 2013) and the MegaMorph project.1

A target list of objects to be fitted can be supplied to GALAPAGOS-2. Objects are fit in descending order of their magnitudes (i.e. brightest first) to ensure that flux contribution of the brightest objects is properly accounted (Häußler et al. 2013). Therefore, for every potential dwarf candidate, we add any objects (detected by SEXTRACTOR) that are brighter and within 150 arcsec of the candidate, to the target list to be fit.

A major consideration for the fitting routine is the PSF used for convolution with the model which is crucial for accurate photometry. An ideal PSF would have a very high signal-to-noise ratio (S/N) with a flat and zero background (Peng et al. 2002). We build a PSF by using a sample of non-saturated stars, requiring that all have a total S/N > 20. All PSFs generated by this method are by default centred at the peak flux and have a zero background. To test the PSF, we inspect the residuals after the PSF is fit to different stars. We use the empirical PSF which have a variety of FWHM values in the different pointings due to the seeing. The sample of stars used to build the PSF are varied to reduce the χ2 goodness of fit.

One of the most common parametric functions used to study light distribution and galaxy morphologies is the Sérsic profile, with the form

\[
I(R) = I_e \exp \left\{ -b_n \left[ \left( \frac{R}{R_e} \right)^{1/n} - 1 \right] \right\},
\]

where \(I_e\) is the intensity at the effective radius \(R_e\), \(n\) is the Sérsic index, and \(b_n\) is a coefficient dependent on the Sérsic index (Graham & Driver 2005). The Sérsic index describes the shape of the profile where the \(n = 1\) case corresponds to an exponential light profile and the \(n = 4\) case corresponds to the de Vaucouleurs profile.

We fit a single component Sérsic model (equation 3) to each of the target list objects. The free parameters for the fit are the position \([x, y]\), total magnitude \(m\), effective radius \(R_e\), the Sérsic index \(n\), the axis ratio \(q = a/b\) (semimajor to semiminor half-axis ratio), and the position angle \(\theta\). For the multiband fitting feature of GALFIT-M, we constrain the free parameters such that only the total magnitude of an object can vary between the \(R\) and \(B\) bands, providing a more robust fit compared to single band fitting. We also perform a GALFIT test run on one of the fields while allowing the structural parameters to vary between the two bands during the fitting process.

1http://www.nottingham.ac.uk/astronomy/megamorph/
As structural properties of galaxies can vary between the two bands, this test run was performed to check if this would have significant effects on the fitted parameters when compared with a run where structural parameters were fixed between the two bands. We find negligible difference in the fitted parameters between the two runs, with significant deviations occurring generally for sources with a high $\chi^2$.

4.2 Image simulations

GALAPagos-2 also outputs uncertainties for each of the free parameters fit to the model. However, the uncertainties calculated by GALFIT are based on Poisson noise statistics and hence are incredibly small and (some debate) even meaningless (Peng et al. 2002). To determine the quality of the fitting and to determine an estimate of the uncertainties of the fitted parameters, we create simulated data on which we run all of our previous processing steps from SExtractor to GALAPagos-2.

The properties of the simulated sample of galaxies were derived using the fits of the dwarf candidates in our fields. The simulated galaxies have magnitudes in $R$ ranging from 16 to 22.5 mag, $\sim$0.5 mag fainter than the magnitude limit of our data to allow us to test the completeness of our methods. The galaxies are distributed within this range using a Schechter luminosity function with a power-law exponent, $\alpha = -1.24$ to obtain a steep luminosity function at the faint end, populated by dwarf galaxies. We only simulate galaxies with Sérsic indices of either $n = 1$ or $n = 4$. The effective radii of the galaxies are scaled according to the size of the faintest galaxy which, we estimate to be $R_e \sim 0.7$ arcsec by extrapolating the effective radius–magnitude relationship of our fitted objects. The remaining free parameters, axis ratio, and position angle are uniformly distributed between 0 to 359$^\circ$, respectively.

We first make a blank image using the sky, gain, and noise properties of one of our fields (F2) to simulate a realistic mimic of the background of our imaging fields. We use a uniform spatial distribution to insert the 120 galaxies with the above properties on the simulated image. We employ a similar method for making a ‘$B$ band image’ for the exact same galaxies by using the median $(B - R)$ colour of real galaxies in our sample to set the magnitude in $B$ band. The PSF is assumed constant across each image, using the PSF from F2 as a template.

To assess the completeness of our method of generating a target list for GALAPagos-2 and the quality of the fit for GALFIT, we perform all of the aforementioned analysis in Section 3 (galaxy detection) and Section 4.1 (galaxy fitting) on the 120 simulated dwarfs. The first pass through SExtractor detects 118/120 galaxies. Implementing the automated dwarf candidate selection criteria described in Section 3.2, we obtain a catalogue of 63 potential dwarf candidates, corresponding to 53 per cent of the detected (by SExtractor) galaxies. The remaining 47 per cent of the galaxies can be split into two groups. First, there are 26 galaxies that are fainter than the magnitude limit of our real data. As our object detection and extraction method is fine tuned to the magnitude and size limit of our imaging data, it is not surprising that those 26 galaxies are not included as potential dwarf candidates by the criteria defined in Section 3.2. Secondly, there are 29 galaxies remaining that are not identified as potential dwarf candidates by our automatic dwarf galaxy selection method. We therefore use this to estimate the completeness of our automatic dwarf galaxy selection method at $\sim 75$ per cent. However, as mentioned in Section 3.2, we visually inspect all of the real images after this automatic selection of galaxies and, we manually add any dwarf candidates that are missed by our selection process.

4.2.1 Quality of the fits

All of the 118 simulated galaxies are subsequently fitted by GALAPagos-2. By comparing the properties of the simulated galaxies with that of the model fit, one can estimate the uncertainties for each of the free parameters in the model. We show in Fig. 3, the deviations of the fitted parameters from the true values, as a function of the fitted $R$ band magnitude. The linear least squares regression fit between the deviation of a parameter and the magnitude, along with the corresponding 1σ confidence intervals are also displayed. The linear fit to the deviation is calculated in the form

$$\text{(Fit}_i - \text{Sim}_x) = a \times m_{R,G} + c$$

where $\text{Fit}_i - \text{Sim}_x$ gives the deviation between the fitted parameter values and the simulated values, computed for each free parameter. $m_{R,G}$ is the fitted $R$ band magnitude, and $a$ and $c$ are the gradient and intercept of the line of best fit, respectively. Generally, the deviations in the parameters get worse at fainter magnitudes, and beyond the magnitude limit of our real images, as shown by the scatter in Fig. 3. However, the opposite is true for the effective radius deviation, which gets worse for brighter, larger objects.

We use the gradient and intercept parameters of the line of best fit to estimate the uncertainty in our fitted parameters. These uncertainties are much more sensible than those calculated by GALFIT although they are likely a lower bound for the true uncertainty. This is because although we use the readout noise, gain, and sky parameters to make an image, inserting galaxies onto each of the imaging fields would provide a more realistic estimate of the uncertainty as any seeing effects or distortions in the real image will be included in the model fit and therefore the uncertainty estimate. In addition, this would also increase the sample size of the simulated galaxies, providing a more robust statistical measure of the deviations from the simulated (true) values. We do not insert the simulated galaxies onto our real images as the crowding becomes too high for our SExtractor configuration to work accurately, which then also affects the GALFIT process.

4.3 Removal of background galaxies

In the absence of spectroscopic data, we employ three criteria based on the morphological and photometric properties of the galaxies in our sample to remove contamination from background galaxies. First, we apply a colour cut such that objects redder than $(B - R) = 2$ are classified as likely background galaxies (Conselice et al. 2002) although, we note that such a cut will also remove any dwarf galaxy members with peculiar stellar populations but these are likely very rare. A colour criteria based on the same principle is found to identify background galaxies in the core of the Virgo cluster (Lieder et al. 2012).

Extensive studies of dwarf galaxies in the LG and clusters (e.g. Binggeli, Sandage & Tammann 1985; Conselice et al. 2002; McGaugh & Sancisi 1992; Binggeli, Sandage & Tammann 1985; Conselice et al. 2002; McGaugh & Sancisi 1992) have found that dwarf galaxies, especially near the central regions, generally have a symmetric elliptical/circular shape and are smooth with no internal structure such as dSphs and dEs. In contrast, background galaxies, especially in the field, can usually be identified visually due to internal structure such as spiral arms, which are visible and resolved at the resolution and depth of...
Figure 3. Analysing the image simulation output using the deviation between GALFIT and simulated values for each major parameter. The deviation for each free parameter is calculated and plotted on the $y$-axis according to equation (4) as a function of the $R$ band fitted magnitude. The subscripts $G$ and $S$ stand for GALFIT output and (initial) simulated values, respectively. The line of best fit, with $1\sigma$ confidence intervals are also included on each plot. The overall low scatter reinforces the efficacy of the galaxy-fitting methodology (see Table 3).

Figure 4. A small set of the galaxy images that are fitted (left), alongside their respective models (middle) and residuals (right). Third row especially shows that we are able to identify spiral galaxies with the resolution of our images. The absolute $R$-band magnitude is printed atop the left tile of each row.

our imaging data. This is evident in Fig. 4 (third row) which shows the model fit process – input galaxy, GALFIT model, and the residuals along each row. Therefore, we study the structural properties by visual inspection of the model and residuals of all the dwarf candidates to remove spirals as likely background galaxies based on the above defined criteria.

Galaxies with asymmetric components such as bulge/disc are not fitted well using a single Sérsic component. This is evident in the residuals and such objects are hence removed from the catalogue as the fitted parameters are likely not reliable.

Then, we refit ‘by hand’ objects with high $\chi^2$ or bad residuals, usually due to the presence of very bright or large stars in the fitting region that are generally not modelled well by the PSF. Such nearby stars were manually masked, and the object refitted before further classification and analysis. Objects which continued to have a bad fit were subsequently removed from further study, as the fitted parameters are likely not accurate. Approximately 22 per cent of the objects were thrown out due to bad fitting. Some of these objects, especially those with highly asymmetric structure are likely to be background systems given their complex morphology as most cluster dwarfs are well fit by a Sérsic profile.

Finally, we study the apparent and absolute size of the galaxies in our sample to constrain the dwarf candidates further. We plot the tight relationship between the central 1 arcsec SB ($\mu_{R,1''}$) and absolute magnitude ($M_{R}^\text{Kron}$) and perform a linear least squares fit to this relationship (blue line; Fig. 5 left) and obtain

$$\mu_{R,1''} = 0.87M_{R}^\text{Kron} + 31.77$$

(5)

to be the best-fitting parameters. SB is independent of distance for non-cosmological distances (which is true for our group). Therefore, a background galaxy can be small in size, but still contain a high SB. Hence, the $\mu_{R,1''} - M_{R}^\text{Kron}$ relationship can be used to assess group...
membership of dwarf candidates. This relationship has been used by others (e.g. Conselice et al. 2002; Müller, Jerjen & Binggeli 2017a; Müller et al. 2017b; Müller, Jerjen & Binggeli 2018a) to identify background galaxies, and in the case of Conselice et al. (2002), identified dwarf galaxies that were later confirmed with spectroscopy by Penny & Conselice (2008). We remove objects which deviate significantly by more than $1\sigma$ from the line of best fit. The tight correlation of the relationship and the lack of clusters of points far from the best-fitting line suggests that our sample is mostly drawn from one distinct population – the galaxy group. This increases our confidence in the effectiveness of the background removal criteria employed.

In Fig. 5 (right), the same line of best fit is shown but as a function of apparent magnitude for objects that were selected to be background by either the colour cut, or the morphological classification criteria. As evident, the scatter about the best-fitting line is larger than for the dwarf candidates as would be expected of background galaxies. Surprisingly, a large fraction of objects selected as background systems lie on/close to the best-fitting line. This may suggest the possible problems with colour-based background selection, as discussed later in Section 4.3.

Also important to note is that the distribution of dwarf candidates revealed no visible clustering, which further suggests that we do not select any background cluster members as dwarf candidates for the NGC-3175 group. In addition, we note that our selection criteria is as conservative as possible in the absence of spectroscopy.

Our resulting catalogue after performing this morphological and colour-based selection consists of 553 dwarf candidates of the group (hereafter, dwarf candidates). In comparison, the final dwarf candidates form $\sim$20 per cent of the 2574 initial potential dwarf candidates from first pass through SExtractor. We show a representative sample of the dwarf candidates in Fig. 6. A truncated catalogue of the dwarf candidates is shown in Table 4 consisting of GALFIT output parameters and the SExtractor area parameter.

However, there are some issues with using colour and morphology to define background galaxies. Conselice et al. (2002) and others have found that there exists a significant population of background galaxies, identified by the presence of peculiar internal or spiral structure, with $(B-R)$ colours $< 2$. Hence, it is likely that there may still be some contamination from background galaxies in our sample, which is inevitable.

5 ANALYSIS

We now investigate the properties of the identified dwarf candidates in the subsequent sections. By analysing which regions exactly these galaxies occupy in key plots such as magnitude-size, and SB-magnitude relations, we can begin to further understand the satellite population of the NGC-3175 group. Prior to this, it is useful to inspect the distributions of each fitted parameter of the dwarf candidates from GALFIT.

Fig. 7 shows the distributions of the parameters fit by GALFIT. Most significantly, most of our objects have Sérsic indices close to $n = 1$, i.e. follow exponential profiles, with a small fraction centred at a de Vaucouleurs profile (with $n = 4$). As anticipated for a dwarf population, the objects are primarily skewed towards the smaller end for effective radii, and towards the fainter end in magnitude. The axis ratio $(b/a)$ spans the entire interval, as do the position angles, with no dramatic spikes nor troughs in their distribution.

5.1 Colour–magnitude relationship

The colour–magnitude relationship (CMR) of dwarf galaxies has been observed and studied in detail, especially for nearby clusters such as Virgo (Binggeli et al. 1985; Lieder et al. 2012), Coma...
Figure 6. Representative sample of dwarf candidates taken from all of our fields with a length of \( \sim 15 \) arcsec on each side. The absolute \( R \) band magnitudes are printed atop each image.

(Adami et al. 2006; Yagi et al. 2016), and Perseus (Conselice et al. 2002). All find the presence of a red sequence, for the bright galaxies \((M_B < -16)\), which identifies the large, passive galaxies. Fig. 8 shows the colour–magnitude diagram for our dwarf candidates (black dots) using the total \((B - R)\) colour. For reference, we also show the dwarf candidates which appeared visually asymmetric (red triangles) and, the objects that were found to contain spiral/discy structure (green cross).

Interestingly, we do not detect very many luminous galaxies in the range where the red sequence is typically fit. At intermediate to faint \((M_B > -12)\) magnitudes, this population of dwarf candidates appears to be an analogue in colour–magnitude space of the low-
mass cluster galaxies (LMCGs) population observed by Conselice et al. (2002) in the Perseus cluster.

### 5.2 Absolute magnitude – effective radius

In Fig. 9, we plot the effective radius of the dwarf candidates versus their absolute $V$-band magnitude, and compare with other dwarf/stellar systems. We do not have $V$-band imaging for our data so, we perform a linear interpolation between the $R$- and $B$-band magnitudes to estimate the $V$-band magnitude for our objects. The literature data of the dwarf and stellar systems are primarily taken from the catalogue compiled by Norris et al. (2014) and the references therein. We show the properties of the MW and M31 dSphs (Walker et al. 2009; McConnachie 2012; Tollerud et al. 2012, 2013), the dE/dS0 sample (Geha, Guhathakurta & van der Marel 2002, 2003; Chilingarian 2009; Forbes et al. 2011; Toloba et al. 2012), the LMCGs (Conselice, Gallagher & Wyse 2003) and, the GCs (Brodie et al. 2011; Strader, Caldwell & Seth 2011) in the size–magnitude plane. Even at our magnitude limit, it is possible to distinguish the GCs (and other compact stellar systems) from the dwarf candidates due to their distinct locations in the size–magnitude plane. The horizontal line shows the initial size limit (based on SExtractor size) employed on our data (see Section 3.2) to remove small objects such as globular clusters. However, after fitting with GALFIT, the sizes of some of the objects changed from their SExtractor measures. As a result some of these objects are now below our initial size limit after fitting. We also find that at the lower end of the size scale SExtractor overestimates the sizes of galaxies from what we find with GALFIT.

We find that our dwarf candidates (filled black circles) appear to follow the scaling relation similar to that of the larger and brighter dEs (hollow green circles) and are close to the dSph area of the size–magnitude relationship. This suggests that our candidates and previous dEs have a similar origin. We also note that our dwarf candidates are significantly smaller in size to the dSphs found in the MW and M31. However, the fitted output of simulated galaxies

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**Figure 7.** Distribution of fitted parameters for the dwarf candidates. These all align as expected for relatively small and faint dwarf galaxies, with Sérsic indices distributed closely around 1 (exponential light profile).
Figure 8. Colour–magnitude diagram for the distinct morphologies of galaxies in our sample along with the red sequence line observed in clusters (Adami et al. 2006). Left: Only the dwarf candidates. Right: Dwarf candidates, dwarf candidates visually identified to have asymmetric structure and objects with spiral/discy structure. The dwarf candidates identified are likely an analogue in colour–magnitude space to the low-mass cluster galaxies (LMCGs) discovered in the Perseus Cluster by Conselice et al. (2002). Unlike in clusters, we do not observe a distinct red sequence in our group, possibly as we do not probe the bright region where the CMR is typically observed.

Figure 9. $M_v$ versus $R_e$ plot for our dwarf candidates (black dots) and literature data, for comparison. Bottom: Scaled to focus on our candidate objects. This more clearly shows the slight overlap with a few GCs, and where the candidates fall close to the dSph/dE locus. Dwarf candidates of the NGC-3175 group are generally smaller than the dwarf galaxies found in both the MW and M31. The horizontal line indicates the initial size limit of our initial selection for the dwarf galaxies. Some galaxies fall below this line after a proper measurement of their sizes with GALFIT (see text). Also shown in the bottom panel is the typical error bar for our dwarf galaxies (the location of the error bar does not represent a real data point). Literature data included on this plot: LG dwarfs (red stars): Walker et al. (2009), McConnachie (2012), Tollerud et al. (2012), Tollerud et al. (2013), and references therein. dE/dS0 (green circles): Geha et al. (2002, 2003), Chilingarian (2009), Toloba et al. (2012), Forbes et al. (2011), GC (blue triangles): Brodie et al. (2011), Perseus LSB (hollow squares): Wittmann et al. (2017), LMCGs (cyan crosses): Conselice et al. (2003).
(Section 4) revealed no systematic underestimation of sizes hence, this relationship is likely not due to our analysis methods. Furthermore, the dispersion in the relationship is small which suggests that our sample is a selection of the faint population and hence we may be missing some of the very large dwarf galaxies. However, we are measuring the sizes of our objects very accurately based on our simulations, and therefore we are likely measuring sizes with a much smaller scatter than what can be done with LG galaxies which suffer from significant contamination due to foreground/background objects.

5.3 Surface brightness – absolute magnitude

We study the SB properties of our dwarf candidates using the accurate shape and size measurements from the Sérsic profile (equation 3) fitting. We make use of calculations from Graham & Driver (2005) to convert from intensity to SB profile $\mu(R)$, given by

$$\mu(R) = \mu_e + \frac{2.5b_n}{\ln(10)} \left( \frac{R}{R_e} \right)^{1/n}$$

(6)

where $\mu_e \equiv \mu(R_e)$ is the SB at the effective radius $R_e$, the Sérsic index $n$ and the related $b_n$ Sérsic coefficient. We make use of an analytical approximation of $b_n$ derived in literature, where $b_n = (2n - \frac{1}{2}) + O(n^{-1})$ (Ciotti 1991).

A special case of equation (6), computed for this investigation, also derived in Graham & Driver (2005), is the ‘mean effective SB’, $\langle \mu_e \rangle$, which is found using the average effective intensity within the radius containing half of the total light

$$\langle \mu_e \rangle = \mu_e - 2.5 \log[f(n)]$$

(7)

where $f(n)$, which describes the profile shape, also depends on the complete gamma function, $\Gamma(2n) = 2 \gamma(2n, b_n)$.

Fig. 10 shows the SB versus magnitude distribution of our sample of dwarf candidates (black circles). For comparison purposes, we also show the region occupied by the LG galaxies (red stars; McConnachie 2012). We also show the region occupied by the low-surface brightness (LSB) galaxies from the Perseus cluster (Wittmann et al. 2017) as hollow squares. LSBs are defined as galaxies with $\langle \mu_e \rangle > 24.8$ mag arcsec$^{-2}$ in $R$ band and the so-called UDGs defined as $\langle \mu_e \rangle \geq 24.8$ mag arcsec$^{-2}$ and $R_e \geq 1.5$ kpc (Yagi et al. 2016) which, have been found to exist in great numbers in clusters (van Dokkum et al. 2015; Koda et al. 2015; Yagi et al. 2016). However, these UDGs are just a subset of dwarf elliptical galaxies found mostly in rich clusters of galaxies (e.g. Conselice et al. 2003; Conselice 2018).

Implementing the above criteria in Fig. 10, we find 53 analogues to the LSB galaxies (green triangles) found in the Perseus cluster core. Recently, a study of abundances of UDGs in lower mass systems, i.e. galaxy groups has been undertaken as part of the Galaxy And Mass Assembly survey (van der Burg et al. 2017), who find that we should expect $\sim 1$ in 5 LG mass analogue systems to contain an UDG. Our results are consistent with the expectations from this study.

5.4 Luminosity function

It has been shown that there exists a tight correlation between the stellar mass-to-light ratio (M/L) and the colours of the integrated light from a galaxy, corresponding to its stellar populations (Bell & de Jong 2001). Bell & de Jong (2001) evolve various formation models with a Salpeter initial mass function (IMF). Among these models, the mass-dependent galaxy formation epoch model, including a burst is found to reproduce the observed local trends in age and metallicity with $K$-band magnitude from Bell & de Jong (2000).

As such, we use the relation:

$$\log_{10} \left( \frac{M}{L} \right) = -0.820(B - R) + 0.851$$

(8)

given by this model to compute the stellar masses of the dwarf candidates.

For our data, we fit a linear function of the form

$$\log(N) = \alpha \log(L) + C,$$

(9)

where $\alpha$ is now the slope describing the shape of the power law and $C$ is a constant. We fit a function of this form to both the luminosity and the mass function as shown in Fig. 11 (left) and (right), respectively. We do not plot any points after incompleteness limit is reached. The error bars are calculated using Poisson statistics. The summary of the slope parameters calculated by this linear fit is shown in Table 5. Both the luminosity and mass functions are not normalized with the volume, however this does not affect the slope parameter $\alpha$, which can be used for comparison with previous studies. We find the faint-end slope $\alpha$ of the LF to be steeper than that observed in the LG.

6 COSMOLOGICAL IMPLICATIONS

We now present the results of our investigation in the context of the missing satellite problem (e.g. Moore et al. 1999). Due to the similarities with the LG, we can compare the properties and the LF of the observed dwarf candidates of the NGC-3175 group with those predicted from numerical simulations of the LG carried out by others easily. We study satellite abundances as a function of stellar masses.

In Fig. 12, we plot the cumulative satellite abundances for the dwarf candidates of the NGC-3175 group (black line). In addition, we also plot the abundances of the observed dwarf galaxies around the MW and M31 (green dot-dashed line) using data compiled by (McConnachie 2012). For simulation data, we overlay a dark matter only (DMO) data set (blue dashed line; hereafter AP04), which comes from the APOSTLE (level AP04) LG simulation (Fattahi et al. 2016) with a resolution of $10^7 M_\odot$. We also show data from the hydrodynamical run of this project (red dotted line; hereafter AP04H). In both cases, we restrict the data to haloes/galaxies within a sphere of radius 500 kpc from the centre of the group. In yellow, we plot the output from a constrained simulation of the formation of MW+M31 (hereafter LG$^C$; Scannapieco et al. 2015; Creasey et al. 2015). Also plotted in cyan are vertical lines to aid with comparisons to our data.

Although the observed satellite abundances in the LG roughly match the output from the AP04H simulation (when not restricted to haloes within 500kpc), the DMO luminosity function is much steeper than the observed. This is expected as not all of the low-mass DM haloes will host a galaxy due to feedback effects, for example, from supernovae. The number of dwarf candidates found at the higher end of masses ($>10^6 M_\odot$) in our sample is lower than that of the observed LG population which suggests that we may be missing some very bright/massive galaxies from our sample, as suggested in Section 5.2. Interestingly, the same is true for all but the AP04H run, which is less steep than our observations at this mass scale. At the depth of our imaging data (low-mass end), we detect $\sim 20$ times more dwarf candidates than galaxies predicted by AP04H run and a factor of $\sim 5$ times more than the LG observations.
NGC-3175 satellites

Figure 10. $\langle \mu_e \rangle_v$ versus $M_V$ for our dwarf candidates with Perseus LSB galaxies (Wittmann et al. 2017) and LG dwarfs (McConnachie 2012, and references therein) plotted alongside. Additionally, we plot the 53 objects in our sample that meet the LSB criteria ($\langle \mu_e \rangle_v \geq 24.8 \text{ mag arcsec}^{-2}$) as green triangles. Also shown is the typical error bar for our dwarf galaxies (the location of the error bar does not represent a real data point).

Figure 11. Power-law fitted to the luminosity function (left) and the mass function (right). The error bars are based on Poisson errors. The luminosity function has a steeper faint end slope than the LG observations with $\sim 5$ times the dwarf galaxies observed than in the LG.

Table 5. The parameters from the linear fit of the form in equation (9) to the mass and luminosity function. The $1\sigma$ uncertainties on the fitted parameters are also shown.

| Function   | $\alpha$       | $C$          |
|------------|----------------|--------------|
| Luminosity | $-1.31 \pm 0.25$ | $10.57 \pm 1.69$ |
| Mass       | $-1.18 \pm 0.07$ | $10.09 \pm 0.54$ |

It is likely that some of our dwarfs are due to contamination and are not true satellite galaxies, but it is unlikely that enough are due to contamination to match the LG abundances given our group membership criteria in Section 4.3. It tentatively appears that at the limit of our data, our abundance observations lie in between a hydrodynamical and a DMO simulation. To resolve the issue of group membership, we are obtaining spectroscopy for some of the dwarf candidates identified in this study.

7 CONCLUSIONS

We identify and study the properties of the dwarf satellite members of the NGC-3175 group (a LG analogue) within its central $\sim 500 \text{ kpc}$ down to $M_B \sim -7.7$. The catalogue of dwarf candidates of NGC-3175 group is used to investigate the missing satellite problem by comparing the observed luminosity function with LG observations and predictions from a range of $\Lambda$CDM simulations.

We use SExtractor to detect dwarf galaxies in our $R$- and $B$-band imaging data (Section 3), fit SB profiles to determine accurate structural properties using GALFIT and, determine the subset of likely dwarf candidates of the group based on the total colour, SB, and morphological visual inspection (Section 4). Through this analysis, we identify 553 dwarf candidates of the group, most of which have never been studied before.

Perhaps unsurprisingly, we find that the dwarf galaxies appear to have similar properties (lower mass, fainter, and smaller) to the LMCGs found near the central regions of clusters (e.g. Perseus: Conselice et al. 2002). The NGC-3175 dwarf galaxies occupy a small region in the size-absolute magnitude plane, showing a change in size by an order of magnitude for a magnitude change of $\sim 5 \text{ mag}$. From this relation, we also find that on average, dwarf candidates from this study are smaller than the dwarf satellites of the MW and M31. This may indicate a possible selection bias that preferentially selects smaller sized dwarf galaxies, or we have measurements which are more accurate resulting in a lower scatter. However, performing the same analysis on simulated images shows no such bias in the output of model fitting. This indicates that the observed trend of smaller sizes dwarf galaxies is likely not due to our analysis but instead has an astrophysical origin.
We study the implications to the standard cosmological model by characterising the luminosity function of the dwarf candidates down to $M_B \sim -7.7$ and compare with observations and simulations of the LG. We find that at the bright end ($M_R < -12$), where there exists a census for LG dwarfs, the abundances of our dwarf galaxy population roughly matches the abundances of LG observations and predictions. However, at the faint limit of our data, we identify more than five times the observed LG satellite population. In comparison with predictions from simulations, our observed satellite abundances lie between a DMO model and a hydrodynamical $\Lambda$CDM model. However, that we detect far more dwarf galaxies than both observations and simulations may be expected if the mass density of our group is different to that of the LG. This can also have an effect on the galaxy sizes of the satellite population, for example, the satellites of M31 are consistently smaller than that of the MW (McConnachie 2012).

Observations of the LG have already found satellite galaxies more than 5 mag fainter than is possible with our imaging data around the NGC-3175 group, making the problem even more severe. Our results suggest that the LG satellite population may not be representative of other groups in the wider Universe. Some of the discrepancy between the observations and simulations may be from contamination due to background objects in our sample. However, it is unlikely that there are enough candidates due to contamination to match the observed LG population after performing our morphological, colour, and SB-based selection of group members.

We are now obtaining spectroscopy for some of these dwarf candidates to determine how many are real dwarf members as opposed to background galaxies which will settle this issue. The spectra will also allow us to measure the mass density of this group to allow a fairer comparison to the LG. Recently, observations have also shown that satellite galaxies lie along a plane in the LG around both the MW (Pawlowski, Pfalz-Alteng & Kroupa 2012; Pawlowski & Kroupa 2013) and M31 (Conn et al. 2013; Ibata et al. 2013), contrary to the expectation of an isotropic distribution of satellites from our understanding of hierarchical structure formation (Ahmed, Brooks & Christensen 2017). Evidence for the existence of a plane of satellites around a system beyond the LG has also been found (Centaurus A: Müller et al. 2018b). However, recent results from Gaia DR2 cast the existence of a plane of satellites into doubt for the LG (Fritz et al. 2018), and thus further work on this topic is needed. Velocity measurements from spectra will also allow us to test this deviation from $\Lambda$CDM for the NGC-3175 group.

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