Are Query-Based Ontology Debuggers Really Helping Knowledge Engineers?

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Abstract
Real-world semantic or knowledge-based systems, e.g., in the biomedical domain, can become large and complex. Tool support for the localization and repair of faults within knowledge bases of such systems can therefore be essential for their practical success. Correspondingly, a number of knowledge base debugging approaches, in particular for ontology-based systems, were proposed throughout recent years. Query-based debugging is a comparably recent interactive approach that localizes the true cause of an observed problem by asking knowledge engineers a series of questions. Concrete implementations of this approach exist, such as the OntoDebug plug-in for the ontology editor Protégé.

To validate that a newly proposed method is favorable over an existing one, researchers often rely on simulation-based comparisons. Such an evaluation approach however has certain limitations and often cannot fully inform us about a method’s true usefulness. We therefore conducted different user studies to assess the practical value of query-based ontology debugging. One main insight from the studies is that the considered interactive approach is indeed more efficient than an alternative algorithmic debugging based on test cases. We also observed that users frequently made errors in the process, which highlights the importance of a careful design of the queries that users need to answer.

Keywords: Knowledge Base Debugging, Interactive Debugging, User Study, Ontologies, Model-based Diagnosis, Protégé, Ontology Debugging Tool

1. Introduction

Systems that are built upon Artificial Intelligence (AI) techniques are often classified into two categories: (i) systems that automatically learn from data and

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systems based on explicitly encoded domain knowledge and automated inference services. Knowledge-based software systems are typical representatives of the latter form of AI with a number of successful applications in various domains such as planning and scheduling, medical advice-giving systems, product configuration, or recommender systems [2, 3, 4, 5, 6].

The correctness of the decisions and suggestions made by a knowledge-based system depends directly on the ability of an expert to formulate and maintain a knowledge base (KB) that describes the application domain. Both knowledge formalization and maintenance can be challenging due to (i) the cognitive complexity of the task and (ii) the size and complexity of the resulting knowledge base—e.g., biomedical ontologies as found on BioPortal\(^1\) sometimes contain thousands of axioms. The results reported, e.g., in [7, 8, 9, 10] suggest that people often make mistakes when writing or interpreting logical sentences. Furthermore, in some cases, knowledge bases are constructed in a collaborative manner by multiple contributors, which is another potential source of faults [11, 12, 13].

Overall, given that unintended or contradictory specifications are likely to occur in such knowledge bases, it is essential to provide experts with appropriate tools for fault detection, localization, and repair. Over the last decades researchers suggested different techniques and implemented a number of assistive tools for these tasks. Many of these techniques are based on the principles of model-based diagnosis (MBD) [14], which is a versatile fault localization method with a range of applications, e.g., in the context of electronic circuits, declarative programs, knowledge bases and ontologies, workflow specifications, as well as programs written in domain-specific and general-purpose languages [15, 16, 17, 18, 19, 20, 21, 22].

In the context of knowledge base debugging, MBD techniques are applied when a knowledge base does not fulfill some basic requirements, e.g., when it is inconsistent in itself or when test cases indicate a failure, i.e., an unexpected output. In the usual MBD problem formulation, test cases are logical sentences that the intended knowledge base must (or must not) entail. The output of an MBD tool is a collection of diagnoses, where each diagnosis corresponds to a set of assumedly faulty parts of the knowledge base. Users of the debugger, such as experts or knowledge engineers, can then investigate one diagnosis after another and inspect the involved components to see if they are faulty or not.

Unfortunately, the number of diagnoses can in some cases be large, e.g., because the information provided by the test cases is insufficient and does not allow the debugger to isolate the true cause of the observed failure. In such cases, already early works suggested asking an expert to provide additional information to narrow down the set of possible fault locations. For example, in the traditional application domain of MBD techniques—electronic circuits—users of a diagnosis system are asked to make additional measurements that give some indication of the health state of certain components [22]. In more recent years, different algorithms for sequential (or: interactive) diagnosis of

\(^1\)http://bioportal.bioontology.org
knowledge-based systems were proposed [13, 23, 24, 25]. Debuggers of this type interactively ask users to provide feedback about the correctness of parts of the knowledge base or certain inferences. One concrete implementation of such a debugger is OntoDebug [26, 27], a plug-in for the Protégé ontology editor [28]. Compared to approaches that solely rely on test cases, the main advantage of such query-based techniques is that they can interactively guide their users to the true cause of the observed problem. In addition, if users always provide correct answers to the debugger’s questions, then query-based diagnosis techniques can guarantee the identification of the true fault location.

The evaluation of sequential diagnosis techniques is usually based on simulations designed to measure, for instance, the time needed to derive the best next query to the expert or the total number of required queries to isolate a fault. Such measures can however have certain limitations when assessing the true usefulness of a debugging approach. In the domain of software engineering, the practical relevance of results obtained with the help of simulation-based evaluations of debugging tools was previously questioned by Parnin and Orso in [29]. In recent years, a number of user studies were therefore conducted that directly assess the usefulness of different academic approaches to tool-supported testing and debugging in the context of software engineering [30, 31, 32].

With the present paper, we continue this line of research. Specifically, our goal was to assess the usefulness of query-based approaches for knowledge base debugging. We correspondingly conducted laboratory studies in the form of testing and debugging exercises that were specifically designed to evaluate if query-based debugging is truly favorable over a previous debugging approach based on test cases. Our corresponding research questions are therefore related to (i) the efficiency and effectiveness of query-based debugging (i.e., do experts need less time, do they find more faults?), (ii) the cognitive ability of users to find out which of the returned diagnoses is the correct one, and (iii) the difficulty of answering system-generated queries for experts.

Among other aspects, our results indicate that a query-based approach can make the debugging process more efficient, without leading to a loss in effectiveness. Furthermore, our experiments and previous studies show that experts sometimes provide wrong answers to the questions of a debugger (“oracle errors”). We therefore conducted additional pen-and-paper studies to develop and validate a prediction model that can be used to estimate the probability of oracle errors based on the cognitive complexity of a query or a test case.

The paper is organized as follows. After discussing previous works in Section 2, we provide the technical background on MBD-based knowledge base debugging in Section 3. Section 4 presents the detailed research questions of our work, and Section 5 and Section 6 discuss the outcomes of our main studies. In Section 7, we finally present first results regarding our prediction model for oracle errors. The paper ends with a discussion of research limitations and a summary of our contributions.
2. Related Work

The process of creating and maintaining a KB is prone to error and—like in standard software development projects—experts can make mistakes when they encode the knowledge about a problem domain. Correspondingly, a number of techniques and tools for KB testing and debugging were proposed over the years. In the following, we first briefly review the main debugging strategies suggested in the literature and then specifically discuss previous works that aim at evaluating the utility of the corresponding tools with the help of user studies.

2.1. General Knowledge Base Debugging Approaches

We can mainly distinguish between model-based and heuristic approaches for KB debugging. Among the model-based approaches, those based on the general MBD principles proposed in [14] are probably the most popular ones. They have, for example, been used to debug ontologies [17, 33, 34], constraints [15, 35], or Answer Set Programming encodings [36, 37].

In case of ontology debugging, MBD methods are used to find sets of axioms, called diagnoses (or: candidates/repairs), that must be modified by a developer in order to formulate the intended ontology. From the technical perspective these methods can roughly be classified in glass-box and black-box ones [38, 39]. Glass-box approaches [40, 41, 42, 43, 44, 45, 46] modify the reasoner such that a single execution run outputs justifications or diagnoses directly. Black-box methods, in contrast, usually apply various search techniques [17, 23, 39, 47] with calls to highly-optimized reasoners for consistency checking and/or the computation of irreducible faulty subsets of an ontology, called justifications or conflicts [34, 35, 48, 49].

In practical settings, given an inconsistent/incoherent ontology, an MBD approach might return more than one diagnosis. In order to restrict the number of obtained diagnoses to only relevant ones, Friedrich et al. [17] suggested the notion of MBD test cases, which were later also used in, e.g., [50, 51, 52]. Each test case is defined as a (set of) axiom(s) that the intended ontology must or must not entail. A debugger can then use these test cases to focus only on those diagnoses for which it is guaranteed that a (suitable) modification of all the axioms of a diagnosis will result in an ontology that satisfies all test cases. However, in many situations, it can be unclear to a developer which test cases should be formulated before the diagnosis session such that a debugger will be able to find the true cause of an unexpected output. In this case, query-based approaches [22, 53, 25, 54] help the user to automatically create test cases. Specifically, the task of the users is reduced to answering a sequence of queries on whether or not the intended ontology must entail a given set of axioms. Assuming that all answers of the developer are correct, a sequential debugger can determine the true diagnosis within the candidates, i.e., the one diagnosis that pinpoints the actually faulty parts of the knowledge base.

Depending on the complexity of the underlying problem, model-based methods can be comparably costly in terms of computation time and space. However,
one main advantage of MBD approaches is that any diagnosis which is returned is a precise and succinct explanation of all identified problems.

In contrast, heuristic approaches to KB debugging, such as [55, 56], are usually based on handcrafted syntactic pattern matching procedures, see, e.g., [9, 57]. Their main advantage is that they allow for fast fault localization in case model-based approaches are too slow. Typically, these debugging procedures are designed to find (combinations of) syntax constructs in a KB that are highly likely to be faulty. Examples of such constructs are, among others, the application of universal role restrictions and disjointness constraints in related ontology axioms [10]. Although these methods are computationally efficient, they are often incomplete (i.e., they can only identify bugs for which appropriate heuristics were defined) and sometimes unsound (i.e., they might return diagnoses that comprise actually correct axioms).

In this paper, we focus on the MBD approach presented in [21, 25], since it (i) provides guarantees about the completeness and soundness of the debugging algorithms and (ii) allows for a precise fault localization by querying its users for additional information.

2.2. Usefulness Analysis of Tools

Since KBs in practice can be large and complex, the research community developed a number of Integrated Development Environments (IDEs) for KB creation and maintenance. Examples of such environments are the MiniZinc IDE for constraint modeling [58], Protégé, which supports the creation of ontologies [59], ASPIDE as a tool for the development of Answer Set Programs [60], as well as various Prolog IDEs like SWI-Prolog [61]. Several of these IDEs come with embedded debugging support or can be extended with external tools like the OntoDebug plug-in used in this paper [62, 63, 26].

Two main approaches exist in the literature to evaluate the usefulness of KB debugging tools. The first one conducts computational analyses providing insights about the usefulness of the tools indirectly. The second form is based on user studies, where the performance and behavior of experts while using the debugger is observed and analyzed. Most of the research in the field is based on the first form of experiments. In comparison to user studies, conducting computational analyses is usually easier, since the only requirement for such evaluations is the existence of a representative collection of knowledge bases that contain real-world or injected faults. Given such KBs, the performance of different debugging algorithms can be compared, for example, in terms of their time and space complexity, the number of calls to the reasoner, the theoretical number of required user interactions, or the precision of the fault localization process. The obtained results can then be used to indirectly assess if a given debugging approach is favorable over another. For instance, we can assume that the reduction of the required computation time increases the usefulness of a system, e.g., because the developer gets faster feedback and can find more bugs in a shorter time.

However, such computational analyses have their limitations. They, for example, cannot be used to determine if certain assumptions made by the eval-
uated debugging methods actually hold. For instance, the interactive ontology debugging method suggested in [25] assumes that a user can decide with certainty if the intended ontology must entail an arbitrary axiom or not. If this assumption does not hold, i.e., the user cannot (correctly) answer all queries of the debugger, the fault localization process might not lead to a unique (correct) result.

User studies can help us to verify such assumptions and can give us additional insights regarding the acceptance and true usefulness of a debugging tool. In the literature, only a few examples of such user studies exist. For instance, the model-based ontology debugging approach proposed in [33] and implemented in the Swoop editor [64] was evaluated by twelve undergraduate and graduate students [41]. The authors’ goal was to investigate if providing justifications for certain inferences can help users find and repair bugs more efficiently. Every subject that participated in the study had at least nine months of experience in ontology engineering and went through an additional 30-minute training session on ontology debugging. The results of the study indicate that tool support in the form of justifications during the debugging process is essential for successful fault localization. However, given the small number of participants, the authors were not able to validate that their results are statistically significant.

Another user study reported in [65] investigated if justifications generated by model-based ontology debuggers can actually be understood by users. Experiments were conducted with 14 undergraduate students and their results showed that justifications can be separated into (cognitively) easy and hard ones. Unfortunately, also in this case the small number of participants did not allow the authors to obtain sufficient statistical evidence to understand why the users find some explanations hard or easy to comprehend.

Finally, a collection of heuristic approaches [9, 10, 66] was studied in [67] and compared with an MBD approach [34]. All 14 subjects participating in the study were educated software engineers and had some experience with ontologies, but no knowledge about hydrology, which was the domain of the study. The task of the participants was to debug and repair an ontology without understanding exactly what it was about. One group of six participants was supported by the MBD approach; the remaining subjects used a heuristic strategy. The obtained results were not fully conclusive. Both participant groups needed about the same amount of time, and no clear preference for either of the approaches was observed. Only for the problem of repairing the ontology, the heuristic patterns helped the subjects to identify bugs more accurately. However, this result must be interpreted with care because the model-based tool did not provide any repair support at that time.

In our work, we continue this line of research which aims to assess the usefulness of debugging approaches based on user studies. Similarly to previous work, we base our user studies on different KBs (ontologies) in which we injected a number of faults. In addition, like in previous research, we involve students in the studies, who have a certain level of education in the development and debugging of ontologies and who received some initial training with the tool. In contrast to previous studies, we were able to recruit a larger number of partic-

6
Participants, which allows us to apply certain statistical analyses. Moreover, we are focusing not on justifications, which are alternative explanations of one fault, but on diagnoses, where each diagnosis provides a potential characterization of all faults in an ontology.

3. Background: Knowledge Base Debugging with MBD

In this section, we outline the main principles of applying model-based diagnosis techniques for knowledge base debugging. We use the particular problem of ontology debugging to illustrate the problem. Ontology debugging was also the task in the user studies reported in this paper, where the participants used the OntoDebug\(^2\) debugging plug-in [26] of the popular ontology editing tool Pro\-tégé [28].\(^3\) The underlying principles and algorithms of the debugging approach are, however, not limited to ontologies and can be applied for various forms of knowledge representation and reasoning, see [21, 68, 62, 69].

3.1. Model-based Diagnosis for Ontology Debugging

In the field of computer science, ontologies are the core of semantic systems. Using a language like OWL [70], they formally describe the relevant concepts in a domain as well as their properties and interrelations. Usually the main goal of semantic applications is to use some form of logic-based reasoning to derive additional facts (entailments) from the given knowledge base.

The starting point for a debugging session is normally when we observe a discrepancy between what we call the intended ontology (denoted as \(O^*\)) and the current version of an ontology \(O\). Such a discrepancy could be the inconsistency of \(O\), the unsatisfiability of its classes, or the presence or absence of certain entailments [26]. In the biology domain, a knowledge engineer might, for example, expect that the ontology-based system is able to deduce from the given axioms that men are animals.\(^4\) If, however, it is inferred, e.g., that men and animals are disjoint, the underlying KB is incorrect and the problem is to find one or more faults in the ontological axioms.

3.1.1. Formal Characterization: Diagnosis Problem

The automated fault localization process starts with the generation of a diagnosis problem instance, which is formally defined as follows [15, 26].

**Definition 1** (Diagnosis Problem Instance (DPI)). Let \(O\) be an ontology (a set of possibly faulty axioms) and \(B\) be a background theory (a set of correct axioms) where \(O \cap B = \emptyset\), and let \(O^*\) denote the (unknown) intended ontology. Moreover, let \(P\) and \(N\) be sets of axioms where \(O^* \cup B\) entails each \(p \in P\) and does not entail any \(n \in N\). Then, the tuple \((O, B, P, N)\) is called a diagnosis problem instance (DPI).

\(^2\)[http://isbi.aau.at/ontodebug/]
\(^3\)[https://protege.stanford.edu/]
\(^4\)[See, e.g., [http://owl.man.ac.uk/2003/why/latest/].]
A diagnosis then is a set of axioms such that the removal of these axioms from the ontology, and the subsequent addition of the background knowledge and the positive test cases, yields a consistent (coherent) ontology that satisfies all test cases.

**Definition 2** (Diagnosis). Let \( \langle \mathcal{O}, \mathcal{B}, P, N \rangle \) be a DPI. Then, a set of axioms \( \mathcal{D} \subseteq \mathcal{O} \) is a diagnosis iff both of the following conditions hold:

1. \( (\mathcal{O} \setminus \mathcal{D}) \cup P \cup \mathcal{B} \) is consistent (coherent, if required)\(^5\)
2. \( (\mathcal{O} \setminus \mathcal{D}) \cup P \cup \mathcal{B} \nvdash n \) for all \( n \in N \)

A diagnosis \( \mathcal{D} \) is minimal iff there is no \( \mathcal{D}' \subset \mathcal{D} \) such that \( \mathcal{D}' \) is a diagnosis.

Different diagnosis computation algorithms exist; they can be distinguished based on whether they generate diagnoses indirectly, i.e., via the computation of conflict sets, or directly, e.g., via divide-and-conquer techniques or through the prior compilation of the problem to an alternative target representation like SAT [14, 21, 23, 39, 72, 73, 74, 75, 76, 77]. In addition, the diagnoses can be ranked (ordered) according to various criteria, such as their cardinality, i.e., number of axioms in a diagnosis, or their likelihood [22]. Such a ranking can simplify the analysis and comparison of diagnoses by allowing the user to focus on the most important ones.

### 3.1.2. Example

We use the following example to illustrate how MBD techniques can be applied to ontology debugging. Let our ontology consist of the following terminological axioms \( \{ax_1 : A \subseteq B, ax_2 : B \subseteq C, ax_3 : C \subseteq D, ax_4 : D \subseteq R\} \). They define that \( A \) is a subclass of \( B \), \( B \) a subclass of \( C \) etc. In a specific domain, this could, e.g., mean that a *MathStudent* is a subclass of *Student*, which is a subclass of *UnivMember*, etc. Further, the ontology contains two assertional axioms \( \{ax_5 : A(v), ax_6 : A(w)\} \), which specify that \( v \) and \( w \) are instances of class \( A \). In a practical application, we could have an assertion like *MathStudent(john)*. Let us assume that the two assertions are known to be correct, and thus should not be considered as fault candidates in the debugging process. To this end, the knowledge engineer would add these axioms to the background theory \( \mathcal{B} \). That is, the ontology would be split into a possibly faulty part \( \mathcal{O} := \{ax_1, \ldots, ax_4\} \) and a correct part \( \mathcal{B} := \{ax_5, ax_6\} \) in this specific case. To make sure that the ontology is correct, we assume the user specifies a set of positive test cases \( P = \{B(v)\} \) and a set of negative test cases \( N = \{R(w)\} \), which means that the intended ontology entails that \( v \) is of class \( B \) and does not entail that \( w \) is of class \( R \).

Unfortunately, the ontology \( \mathcal{O} \), together with the correct axioms \( \mathcal{B} \), entails \( R(w) \), i.e., \( \mathcal{O} \cup \mathcal{B} \models R(w) \), since \( A(w) \) holds and \( A \) is transitively a subclass of

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\(^5\)An ontology \( \mathcal{O} \) is coherent iff there do not exist any unsatisfiable classes in \( \mathcal{O} \). A class \( X \) is unsatisfiable in an ontology \( \mathcal{O} \) iff, for each interpretation \( \mathcal{I} \) of \( \mathcal{O} \) where \( \mathcal{I} \models \mathcal{O} \), it holds that \( X^{\mathcal{I}} = \emptyset \). See also [71, Def. 1 and 2]
Now, given the specified DPI \(⟨O, B, P, N⟩\) as an input, a debugging system will identify the following four minimal diagnoses: \(D_1 : [ax_1]\), \(D_2 : [ax_2]\), \(D_3 : [ax_3]\), and \(D_4 : [ax_4]\).

The intuitive explanation why we get these diagnoses is that the removal of any individual axiom in \(O\) would break the subclass relationship chain, and the undesired entailment \(R(w)\) would not be present anymore.

However, based on the positive and negative test cases alone, an MBD algorithm cannot discriminate between the four diagnoses, and we cannot derive the true cause of the problem. The user can therefore either inspect all diagnoses manually, or provide more information, e.g., in terms of additional test cases.

Assume that the user specifies an additional negative test case \(B(w)\). With \(N = \{R(w), B(w)\}\) and \(P = \{B(v)\}\), a debugger will return \(D_1\) as the only minimal diagnosis. Because, the modifications suggested by the sets of axioms \(D_2, D_3,\) and \(D_4\) leave \(ax_1\) untouched, and \(ax_1\) in conjunction with \(A(w) ∈ B\) leads to the entailment of \(B(w)\), and thus to a violation of the negative test cases.

However, the modified ontology \(O_1 := O \setminus D_1\) now does not entail the positive test case \(B(v)\) anymore. Therefore, \(O_1\) must be extended somehow. Since the debugger cannot know how to correctly extend the knowledge base, one strategy is to use the required entailments \(P\) explicitly as an extension [21]. Hence, in our example, one would simply add \(B(v)\) to \(O_1\).

### 3.2. Sequential Diagnosis

As the example shows, additional knowledge (in our case, test cases) can help to further focus the debugging process and rule out possible fault candidates. Not all test cases are, however, equally helpful. One of the goals of sequential diagnosis is therefore to automatically identify “good” or optimal test cases, and to interactively ask the user (or some other oracle) to classify the generated test cases as either positive (intended entailment) or negative (non-intended entailment). We call such a (set of) test case(s) selected by the system and shown to the user for classification a query. Based on the user’s answer, the debugger can then update its knowledge in terms of the positive and negative test case sets and repeat the process until only one single diagnosis remains.

#### 3.2.1. Formal Characterization: Oracle and Queries

The notions of an oracle and a query can formally be described as follows. An oracle categorizes elements of a set of axioms either as positive or negative test cases by checking if the intended ontology must or must not entail these elements.

**Definition 3** (Oracle). Let \(Ax\) be a set of axioms. Furthermore, let \(\text{ans} : Ax → \{P, N\}\) be a function which assigns axioms in \(Ax\) to either the positive or the negative test cases. Then, we call \(\text{ans}\) an oracle w.r.t. the intended ontology \(O^*\), iff for any \(ax ∈ Ax\) both of the following conditions hold:

\[
\begin{align*}
\text{ans}(ax) = P & \implies O^* ∪ B \models ax \\
\text{ans}(ax) = N & \implies O^* ∪ B \not\models ax
\end{align*}
\]
Note that the function \( \text{ans} \) can either be total or partial. In the first case, the oracle (user) is a full domain expert and able to classify all queried axioms; in the latter case, there might be axioms that the oracle is not able to classify.

Since our goal is to narrow down the set of possible diagnoses, a debugger should propose only queries that guarantee the acquisition of relevant information. In other words, each query should eliminate at least one diagnosis, given any answer of a full domain expert. Generally, a query consists of one or more axioms and can be characterized as follows.\(^6\)

**Definition 4 (Query).** Let \( \langle O, B, P, N \rangle \) be a DPI, \( D \) be a set of diagnoses for this DPI, and \( Q \) be a set of axioms. Moreover, let \( Q^P_{\text{ans}} := \{ q \in Q \mid \text{ans}(q) = P \} \) and \( Q^N_{\text{ans}} := \{ q \in Q \mid \text{ans}(q) = N \} \) denote the subsets of \( Q \) assigned to \( P \) and \( N \) by an oracle \( \text{ans} \).

Then we call \( Q \) a query for \( D \) iff, for any classification \( Q^P_{\text{ans}}, Q^N_{\text{ans}} \) of the axioms in \( Q \) of a full domain expert oracle \( \text{ans} \), at least one diagnosis in \( D \) is no longer a diagnosis for the new DPI \( \langle O, B, P \cup Q^P_{\text{ans}}, N \cup Q^N_{\text{ans}} \rangle \).

Different strategies were proposed in the literature to determine “good” or optimal queries, see, e.g., [22, 79, 80]. Usually, this is accomplished by computing a set of diagnoses and by analyzing the effects of applying the different diagnoses with respect to a potential query. Complementary to this approach, a recent work suggests novel ways of diagnosis computation to reduce the user’s time and effort for query answering [72].

In general, a byproduct of the process of determining the queries is a quality estimate for each resulting query. Such a quality measure can, for example, be based on the expected information gain after the user has answered the query [22], on reinforcement learning [81], or on criteria [54, 82, 83] adopted from the field of active learning [84]. Finally, since the generation of queries requires potentially costly calls to an underlying reasoner, approaches exist that aim to minimize the number of these computations [21, 68, 85, 54].

### 3.2.2. Example

One way to assess the utility of different possible test cases—which in the end correspond to queries to the user—is to analyze the entailments of the ontologies \( O^*_i := (O \setminus D_i) \cup P \) after the application of the different diagnoses \( D_i \).

In our example from above, the four ontologies \( O^*_1, \ldots, O^*_4 \) have, among others, the following entailments:

\[
O^*_1 : \emptyset, \quad O^*_2 : \{B(w)\}, \quad O^*_3 : \{B(w), C(w)\}, \quad \text{and} \quad O^*_4 : \{B(w), C(w), D(w)\}
\]

\(^6\)Whenever we speak of a “query” throughout this work, we mean a query in terms of Definition 4, which must not be confused, e.g., with the concept of a query in terms of a query language such as OWL-QL [78]. In our scenario, queries are answered based on the knowledge of an oracle about the intended ontology, with the aim to locate faults in an ontology. Queries in terms of query languages are answered based on the knowledge specified in an ontology, knowledge graph, etc., in order to find answers to questions of relevance.
These entailments can be obtained, e.g., with the help of the realization service of a Description Logic reasoner and can serve as test cases.

Let us assume that the user knows that $D(w)$ must be entailed and adds it as a positive test case, i.e., the diagnosis problem instance is now

$$DPI = \langle \mathcal{O}, \{A(v), A(w)\}, \{B(v), D(w)\}, \{R(w)\} \rangle$$

Given this additional information, a model-based debugger will return only one single diagnosis, $D_4 = [ax_4]$. All other diagnoses that existed for the problem instance without the new test case, are no longer minimal diagnoses. Specifically, the deletion of each of the diagnoses $D_1$, $D_2$, or $D_3$ from $\mathcal{O}$ does not affect $ax_4$, which is however—due to $D(w) \in P$—responsible for the unwanted entailment $R(w) \in N$.

Sequential diagnosis algorithms usually make analyses of this type to determine queries (test cases) that are likely to narrow down the set of remaining diagnoses. At the end, the user only has to categorize such system-generated queries and acts as an oracle for the debugger.

### 3.3. The OntoDebug Plug-In to Protégé

The described concepts for sequential and test case based MBD for ontologies were implemented in the OntoDebug plug-in of the widely-used Protégé ontology editor. There are two main situations when the user of the tool—possibly after some maintenance activities—might initiate a debugging session with the OntoDebug plug-in. First, the built-in reasoner of Protégé might detect that the given ontology is faulty, e.g. inconsistent or incoherent, in itself. In contrast to other application areas of model-based diagnosis techniques—such as fault localization in electronic circuits—inconsistencies can be present in the context of ontology debugging problems without any initially given test cases (observations).

Second, even if the ontology in itself is consistent and coherent, the user might want to ensure that the implemented ontology corresponds to the intended one by specifying one or more test cases. If the test cases lead to the disclosure of unexpected entailments, an inconsistency or an incoherency, it is obvious that something is wrong with the ontology.

One possible first step for the user when starting the debugging process with OntoDebug—indeed of how the user detected that there is a problem—is to tell the system which parts of the ontology are definitely correct (and thus are a part of the background knowledge). This task can be accomplished using the functionality at the right-most side of the user interface of OntoDebug shown in Figure 1. In this example, the user works on problems of the “Koala” ontology of the Protégé project, an ontology that was created for educational purposes which contains typical problems that can occur during ontology development. Specifically, in the example, the user has declared among other things that the axiom “BA (bachelor of arts) is of type Degree” is definitely correct.

Once this optional step is done, the user can start the model-based debugging process. To this end, the tool, as mentioned above, supports two general strategies.
First, the user can inspect the list of diagnoses returned by OntoDebug to locate the fault and add additional test cases if the list of diagnoses contains too many elements. Generally, the idea is that the provision of additional, carefully designed test cases will help to narrow down the set of possible diagnoses, i.e., the possible causes for the problems in the ontology. In the example shown in Figure 1, the user has specified one positive test case ("Student is a subclass of Person") and a negative one ("Person is a subclass of Marsupials"), using the sub-window in the middle of the screen.

The second supported debugging strategy is the query-based one. In this case, the tool will—based on the inconsistent (incoherent) ontology or the failing test cases—compute the first query to the user. In our example, the system determined a query consisting of two axioms shown in the top-left sub-window of the user interface. The two axioms to be categorized by the user are "KoalaWithPhD is a subclass of Koala" and "KoalaWithPhD is a subclass of Person." The user can answer the query by using the green and red plus and minus symbols (or leave some axioms uncategorized), and then submit the answer to the system. The system adds the user’s feedback to the “Acquired Test Cases” and then restarts the computations using the additionally provided information. In case the information was sufficient to...
identify a single diagnosis as the cause of the problem, the user is pointed to the faulty parts of the ontology. Otherwise, the system computes a new query to the user and the cycle repeats until only one diagnosis remains.

Generally, one main difference is that in the approach based on test cases the users have to think by themselves about good test cases, while in the case of interactive debugging, user responses to the system-generated queries are taken as additional test cases. In this latter case, the selection of the query, and correspondingly the test case(s), is based on an internal reasoning process that ensures that the most informative queries are chosen.

4. Research Questions

The main promise of interactive, query-based approaches is that they are able to systematically guide users (e.g., knowledge engineers or domain experts) through the debugging process and that after the interactive process the true cause of the observed discrepancies is found. In contrast, there is limited support for users in the more traditional model-based debugging setting, where the users have to provide test cases manually in order to incrementally narrow down the set of fault candidates.

As discussed in Section 2, computational analyses—such as measurements of time or an analysis of the number of required queries—can be insufficient to inform us about the usefulness and acceptance of the corresponding tools, and cannot tell us in which ways query-based debugging is advantageous over a test case based approach.

To address these open questions, we conducted a number of controlled (laboratory) studies, mainly consisting of ontology debugging exercises. We focus on the following main research questions in the context of model-based debugging:

RQ1 Is the debugging process more effective when users are supported by a query-based debugging tool than when test cases are the only means to locate faults?

RQ2 Is the process more efficient when users are supported by a query-based debugging tool?

RQ3 To what extent do the assumptions of MBD debugging techniques hold?

RQ3.1 For the case of approaches based on test cases and candidate ranking: Do users have “perfect bug understanding”, i.e., do they reliably recognize the true cause of a discrepancy within a list of diagnoses?

RQ3.2 For the case of the query-based approach: Do users make errors when acting as oracles?

The following studies were designed and executed.
• In our preliminary study (Study 1), our goal was to gauge the general usefulness of a test case based debugging approach. We specifically also explored the importance of the ranking of the fault candidates in this experiment (RQ3.1). The study also served us to further improve the design of the main study (Study 2).

• In Study 2, we investigated the effectiveness and efficiency of the query-based and the test case based debugging approach (RQ1 and RQ2). In that context, we also examined the question of oracle errors (RQ3.2).

Additional pen-and-paper studies were conducted in the context of both Study 1 and Study 2 with the goal of deepening our understanding of the (types of) errors that occur while debugging. These insights are then used to devise a heuristic prediction model for such errors (RQ3.2). We discuss Study 1 in Section 5, Study 2 in Section 6, and the additional studies in Section 7.8

5. Study 1: Investigating MBD-debugging With Test Cases

5.1. Design of the Pre-Study

5.1.1. Task

The task of the participants in this study was to find the faulty axioms (true diagnosis) in a given faulty ontology (i) based on a provided description of the intended ontology in natural language (ii) using the OntoDebug tool described above (iii) by creating test cases manually (the query-based debugging functionality was not available to the users). The participants were explicitly instructed to (iv) constantly inspect the list of possible diagnoses throughout the debugging session and to (v) mark the true diagnosis once they detected it in the list. After a diagnosis was marked, the debugging session ended. In Figure 1, the list of diagnoses is shown in the bottom-left sub-window labeled with “Possible Ontology Repairs”.

5.1.2. Ontologies

In order to make sure that the outcomes regarding the usefulness of the test case based debugging approach do not depend on the specifics of a certain ontology, two different ontologies describing two different domains were used in the study. The first one corresponded to a (simplified) model of our university (university domain) and the second one was a real-world knowledge base made available to us by the “Communal IT Center of Carinthia” (IT domain). We prepared the ontologies for the study by injecting five faults into each of them such that the resulting ontologies were inconsistent and incoherent in themselves. That is, for both ontologies the true diagnosis included five faulty axioms (as

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8The (anonymized) raw data obtained throughout Study 1 and Study 2 as well as the ontologies used in the experiments can be downloaded from http://isbi.aau.at/ontodebug/evaluation.
shown in Table 1). The designed ontologies were similar in size and complexity. For example, both included about 50 classes, 90 subclass relationships, and 20 object properties. Moreover, both included roughly equally complex logical formalisms and used the full expressivity of the Description Logic $\mathcal{SROIQ}$ [3, 88] or, respectively, OWL 1.1 [89].

Table 1: Faulty ontology axioms (university domain) in OWL Manchester Syntax [90].

| Nr. | Faulty Axiom |
|-----|--------------|
| 1   | Department SubClassOf offers only Course |
| 2   | Library SubClassOf offers only Visitation |
| 3   | Research_Event SubClassOf has_Speaker only (Person and (has_Degree some Degree)) |
| 4   | Assembly_Hall DisjointWith Room |
| 5   | Department DisjointWith Room |

5.1.3. Participants

We recruited 29 participants for the study. All participants were computer science students of our university and were enrolled in an ongoing master program course on knowledge engineering. During this course, the participants, who already had a background in logics, were introduced to model-based debugging, formal ontologies, Description Logics, and the OWL language. The participants also had first experiences in designing ontologies with Protégé and debugging them with OntoDebug. Overall, the participants were very homogeneous with respect to their knowledge and background.

5.1.4. Independent Variables

We considered two independent variables, the ontology to be debugged (university vs. IT) and the position (visible vs. not visible) of the true diagnosis in the list of diagnoses returned by the debugger. Each participant was randomly assigned to one ontology and one of two configurations regarding the position of the true diagnosis.

Similar to the work in [29], we varied the position to assess the importance of the ranking of the diagnoses returned by the system. Specifically, in the visible case, the true diagnosis, which comprised all actually faulty axioms of the ontology, was placed within the top three diagnoses and was therefore always visible to the user. In the other case (not visible), the true diagnosis was further down the list. Generally, the diagnosis problem was designed in a way that the initial list of diagnoses (before further test cases are specified) is comparably large, including over 150 diagnoses in each case.

5.1.5. Dependent Variables

We made a variety of automated, objective measurements while the participants were executing the task, like the needed time, the number of user interactions (mouse clicks) in the debugger, and the number of diagnoses still in the list
of diagnoses when the participants submitted the diagnosis which they thought is the correct one. In the context of Study 1 the most important automated measurement was on the correctness of the debugging process in terms of (i) the fraction of correctly identified faulty axioms and (ii) the fraction of users who correctly identified all five faulty axioms (i.e. the true diagnosis).

Moreover, the participants had to specify their subjective degree of belief (confidence) in having solved the fault localization task correctly. For this, they were instructed to use a range between 0 (certain that the marked diagnosis is not the true one) and 100 (certain that the marked diagnosis is the true one).

5.2. Experiment Execution

The study was conducted in one of the computer labs of our university. The required software was pre-installed on the lab computers. All of the computers were identically equipped. After being informed about the tasks of the study and after the participants had declared their consent, they were provided with detailed material on paper. The handout essentially included a description of the domain that was incorrectly modeled by the ontology the participants had to debug. Thus, the paper characterized the intended ontology as discussed in Section 3.

The description was given as a natural language text, with important concepts highlighted. In particular, class and property names in the ontology were italicized and underlined, respectively. An example of such a description from the university domain is the following:

From an organizational point of view, the University is subdivided into several OrganizationalUnits. Each OrganizationalUnit employs some OfficeEmployee(s) and some Teacher(s), has some Room(s) which is/are (an) Office(s), is directed by exactly one Director and is located in some Building. Two special types of OrganizationalUnits are the Directorate and the HumanResourcesUnit.

Before the participants started their task, they received another brief tutorial on how to debug an ontology with the OntoDebug tool. They used the “Koala” ontology that is available in Protégé (cf. Sec. 3.3) for that purpose. During the experiment, the participants were not allowed to talk to each other. The participants were supervised by three instructors, who were present to answer questions in case of problems with the software.

5.3. Outcomes of Study 1

The measurements obtained in Study 1 are summarized by Figures 2 and 3. As mentioned above, the main question of this pre-study was (i) to gauge the general usefulness of MBD-debugging with test cases and (ii) to assess the importance of the ranking of the diagnoses. Furthermore, a side goal was to obtain experiences regarding the study design for the main study (Study 2).
5.3.1. General Usefulness of Model-based Debugging

On average, the participants took about 28 minutes and 81 mouse clicks for the task before they submitted their solution. Overall, the participants correctly identified as many as 77% of the problematic axioms, i.e., almost four out of the five injected faults shown in Table 1 were eliminated. From the 29 participants, 10 (34.4%) correctly identified the true diagnosis, i.e., all five faulty axioms (cf. Figure 2).

Overall, we find this result very positive, given the complexity of the task. The study clearly indicates that model-based debugging is actually helpful for knowledge engineers. Since we did not observe any statistically significant differences between the observations that were made for two different ontology debugging problems (university and IT), we are confident that the usefulness of the approach is not limited to just one domain.

There were various reasons why some participants did not successfully find all faults. A main issue appeared to be a certain lack of attentiveness and precision when reading the natural language specification of the intended ontology. Based on these observations, we revised some of the specifications, e.g., by removing possible ambiguities, when designing Study 2. To a certain extent, it also seemed that some participants did not properly understand the semantics of certain elements of the knowledge representation language.

5.3.2. Importance of Ranking of Candidates (RQ3.1)

In the context of RQ3.1, our goal was to investigate if the capability of a debugger to rank the true diagnosis higher in a list of candidates directly translates into a more effective debugging process. Table 2 shows in how many cases the true diagnosis—which comprises all five injected faults—was found, depending on whether it was among the top-ranked (visible) candidates or not.

Table 2: Relationship between full correctness of the debugging task and visibility of the true diagnosis in the list of diagnoses presented to the participant.

| true diagnosis visible | yes | no |
|------------------------|-----|----|
| true diagnosis found    | yes | 5  | 5  |
|                        | no  | 9  | 10 |

Interestingly, the observations shown in Table 2 do not provide evidence that the users were more effective when the true diagnosis was always visible. Such a non-effect of varying the position of the fault in a ranked list was also reported in [29].

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9 The standard deviation was 12.6 minutes (time) and 35 mouse clicks, respectively.
10 The standard deviation was 21%.
11 Note, in Figures 2 and 4 we use line and area charts (instead of, e.g., bar charts or dot plots) for reasons of clarity and better distinguishability between the plotted variables, although the x-axis is in fact a categorical axis.
12 This is supported by Fisher’s Exact Test [91] (p-value = 1.00).
Figure 2: Overview of the outcomes of Study 1. The figure shows the measurements for the dependent variables for all 29 debugging sessions, grouped by the position (“visible” left, “not visible” right) of the true diagnosis in the diagnoses list, and sorted from low to high confidence. The labels along the x-axis indicate whether the true diagnosis was found (“Y”) or not (“N”) during the respective session. Variables plotted w.r.t. the right y-axis are underlined. The numbers (ranging from 1 to 36) in the plot indicate the exact value of the “# of diagnoses still in list” variable.

Figure 3: Violin plots showing the distribution of the dependent variables in Study 1.

Moreover, 10 of the 14 participants of the group where the true diagnosis was ranked highly continued specifying test cases until only one diagnosis was left in the list (cf. Figure 2)—even though all participants were explicitly instructed to constantly inspect the list of diagnoses and mark the true diagnosis once they detected it in the list. A large number of participants therefore did not recognize the actual fault even though it was shown to them.

These findings challenge the assumption of a “perfect bug understanding” of the users, i.e., they do not always immediately identify a fault when they are pointed to it. In other words, even if the true diagnosis was visible to the participants, they (i) did not recognize it in the majority of the cases and (ii) did not identify it more often than other participants to which the true diagnosis was not (always) visible. As a result, fault ranking metrics should not be considered as the only measure when different algorithmic debugging
strategies are compared [29].

5.3.3. Additional Observations (Study 1)

Positive test cases are more reliable: From the 244 test cases provided by the participants (8 on average per debugging session), the majority (71%) were positively formulated, i.e., they described required entailments. The participants therefore seemed to feel more comfortable specifying things that must be entailed than those that must not. An analysis of the fault rates for positive and negative test cases indeed confirmed that negative ones, i.e., formulated non-entailments, were significantly more often faulty (24% vs. 10%, see Table 3). This result suggests that it can be better to ask users questions with a bias towards the positive answer in query-based KB debugging, in order to minimize oracle errors.

Table 3: Relationship between the type of formulated test case and its faultiness.

| type of test case | positive | negative |
|-------------------|----------|----------|
| test case faulty   | yes      | 18       | 17       |
|                   | no       | 156      | 53       |

Users can be overconfident: The participants of the study were, on average, overconfident (cf. Figure 2). That is, the average confidence value expressed by the participants regarding the correctness of the identified diagnosis was at about 83% (cf. Figure 3) whereas only 34% of them have correctly located the true diagnosis. In other words, the average self-reported confidence of users in their own success overestimates the actual user success rate. Interestingly, the confidence of those participants who did not find the true diagnosis was even slightly higher than the confidence of the successful participants.

Overall, this can be seen as an indicator that subjective confidence estimates have to be handled with care [81] when they are intended to be used to guide the debugging process [25].

Users consider themselves as imperfect oracles: We found that only 31% of all users, and an even lower 20% of the ones that successfully found all faults, were fully confident about the correctness of their debugging actions (cf. Figure 2). This teaches us that humans generally do not regard themselves as perfect oracles for knowledge engineering tasks, which questions the frequently made “perfect oracle” assumption. We pick up on this discussion again in Sec. 6.3.4 and Sec. 7.

Completion time and user activity as success predictors (cf. Figure 2): Participants who correctly identified the true diagnosis required on average more time

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13 According to a (two-tailed) Fisher’s Exact Test with α = 0.01 (p-value = 0.008).
14 A “bias towards the positive answer” means that the estimated probability of getting a positive answer to the question is higher than that of a negative answer.
15 In all the presented violin plots, the white dot indicates the median and the thick box ranges from the first to the third quartile.
(33 minutes) and specified more test cases (10). However, they needed fewer interactions (71 clicks) than those who submitted a wrong diagnosis (26 minutes, 8 test cases, 87 clicks). This indicates that successful users worked more thoroughly and were more persistent in their testing activity. Unsuccessful ones, in contrast, required more interactions as they more frequently edited, deleted or re-added test cases. An atypically high editing activity can thus be considered as an indicator that a user requires more assistance for the given task.

6. Study 2: On the Usefulness of Query-based Debugging

Having established that model-based debugging leads to a good debugging performance, the goal of Study 2 was to answer our main research questions RQ1 and RQ2 on the efficiency and effectiveness of query-based debugging as opposed to a test case based approach. In other words, do users need less time/effort when supported by a query-based debugger (efficiency) and do they find more faults (effectiveness)?

6.1. Design of the Study

6.1.1. Task

As in the pre-study, the general task of the participants was to find the actually faulty axioms (true diagnosis) in given faulty ontologies (i) based on a description of the intended ontology in natural language (ii) using the OntoDebug tool. However, now (iii) every participant had to debug two ontologies, one using the query-based and the other using the test case based approach.

6.1.2. Ontologies

Similar ontologies were used as in the pre-study—one describing a university, and one describing an IT domain, and both again corresponding to the Description Logic $\text{SROIQ}$. We prepared the ontologies for the study by injecting a number of faults into each of them, leading to both inconsistency and incoherency, similarly as in Study 1. However, the ontologies were roughly 20\% larger in terms of their size (e.g., number of axioms and classes) than the ones used in Study 1; still, the size and complexity of both ontologies was roughly equal. The ontologies were enlarged to achieve a higher number of fault candidates. Concretely, the size of the initial list of diagnoses for both ontologies was now over 1000. This made the diagnosis problems objectively harder than in the pre-study. The reason for this was to compensate for the lower number of participants (23) in Study 2, which makes it more challenging to achieve statistically significant results. In fact, if any effects (e.g., regarding time or user interactions) of employing the query-based debugging method can be found, then they are likely to be larger for harder debugging problems.
6.1.3. Participants

For Study 2, we could draw on 23 participants. Again, all of them were attendees of a university master program course on knowledge engineering. However, the focus of the course was now shifted towards Semantic Web technologies to achieve a better preparation of the students for the study. As a consequence, the participants of Study 2 had a better education on model-based diagnosis, formal ontologies, ontological reasoning, and the used knowledge representation language than those of Study 1. Moreover, they had more experience with Protégé and OntoDebug.

6.1.4. Independent Variables

The two independent variables we used were the ontology to be debugged (university vs. IT) and the debugging strategy (query-based vs. test case based). We used a within-subjects experiment design in this study, which involves each participant consecutively working on both ontologies and consecutively using both debugging strategies. Thus, we randomly assigned each participant to one of the following configurations:

- Task 1: university with queries. Task 2: IT with test cases.
- Task 1: university with test cases. Task 2: IT with queries.
- Task 1: IT with queries. Task 2: university with test cases.
- Task 1: IT with test cases. Task 2: university with queries.

6.1.5. Dependent Variables

In terms of measurements, we recorded the same aspects as in Study 1 (see Section 5.1.5), i.e., time, number of user interactions, number of diagnoses still in the list, correctness (fraction of faulty axioms found, fraction of users finding the true diagnosis), and confidence.

6.2. Experiment Execution

The experiment execution was exactly the same as in Study 1, see Section 5.2.

6.3. Outcomes of Study 2

6.3.1. Effectiveness of Query-based Debugging (RQ1)

To assess the effectiveness of the two debugging strategies, we analyzed how many of the faulty axioms were successfully identified by the participants. Across both ontologies, the participants on average found 91.3% of the faults when they were supported by the query-based debugger and 89.1% when the debugging process was based on test cases (as in Study 1). The differences were not statistically significant. We therefore conclude

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16 The random variation of the order of the tasks is important to avoid systematic learning effects.
17 The standard deviation amounts to 19% (queries) and 23% (test cases).
Figure 4: Overview of the outcomes of Study 2. The figure shows the measurements for the dependent variables for all 46 debugging sessions (2 per user), grouped by the used debugging strategy (“queries” left, “test cases” right; i-th x-axis entry starting from the left in the “queries” block refers to the same user as i-th x-axis entry starting from the left in the “test cases” block). Records are sorted by the number of mouse clicks of the “test cases” sessions from low to high. The labels along the x-axis indicate whether the true diagnosis was found (“Y”) or not (“N”) during the respective session. Variables plotted w.r.t. the right y-axis are underlined. The numbers (ranging from 1 to 26) in the plot indicate the exact value of the “# of diagnoses still in list” variable.

that in this experiment the query-based approach did not further increase the effectiveness of the debugging process.

Note, however, that in both cases the success rate was higher than in Study 1, where 77% of the faults were identified by the participants. We attribute this to the fact that—based on the learnings from Study 1—we were more successful in motivating the participants to work more carefully. In addition, the participants of Study 2 were, as mentioned, better trained in ontology engineering than those of Study 1. As a result, it became difficult to greatly increase the already high success rate (89.1%) obtained by participants who relied on test case based debugging.

Like in Study 1, we also analyzed how many of the participants could correctly identify all faulty axioms (i.e. the true diagnosis) in each ontology. We again found no statistically significant difference between the two debugging approaches (cf. Table 4). Generally, across the ontologies, the fraction of fully successful trials was much higher than in Study 1. About 72% of the participants were able to find all problems in the respective ontologies. Interestingly, we registered a non-conformity between the two ontologies this time. Over 85% of the participants were able to find all faults in the university ontology, with no significant differences with respect to the debugging method. However, in the IT domain, only 57% were fully successful. A potential reason for this result could lie in the prior knowledge of the participants with regard to the two domains. More research is however required to better understand this phenomenon.
6.3.2. Efficiency of Query-based Debugging (RQ2)

To assess if the query-based debugging technique helps users to accomplish the debugging task faster and with less effort, we compared both the overall time needed by the participants and the number of required user interactions (mouse clicks) in the debugging tool across the two debugging strategies. The (distribution of the) time and user interaction measurements throughout Study 2 is summarized by Figures 4, 6 and 7.

Participants who were supported by the query-based debugging tool on average needed 24.9 minutes. When using test cases without query support, the average time was 34.0 minutes, which amounts to an overhead of 37%. Looking at the number of required user interactions, the differences are even stronger. With the query-based debugging tool, the number of mouse clicks was more than halved and reduced from about 139 to 64 clicks on average.

The differences regarding both time and interactions were statistically significant according to a Wilcoxon Rank-Sum Test;\textsuperscript{20} in the case of time to the level $\alpha = 0.05$ (p-value $= 0.0418$), and for clicks to the level $\alpha = 0.00001$ (p-value $< 0.00001$).\textsuperscript{21}

Overall, we conclude from the experiments that query-based debugging sup-

\begin{table}[h]
\centering
\begin{tabular}{|l|c|c|}
\hline
true diagnosis found & queries & test cases \\
\hline
yes & 17 & 16 \\
no & 6 & 7 \\
\hline
\end{tabular}
\caption{Relationship between the used debugging approach and the success in finding the true diagnosis.}
\end{table}

\footnote{The standard deviation comes to 11 minutes (queries) and 19 minutes (test cases).}
\footnote{Standard deviation: 25 clicks (queries) and 90 clicks (test cases).}
\footnote{Since literature is not always consistent when referring to Wilcoxon’s test(s), note that we stick to the description of the test(s) given in [91]. Further note that Wilcoxon’s Rank-Sum test compares independent samples whereas Wilcoxon’s Signed Rank test compares paired data.}
\footnote{Also, when viewing the data as paired (each participant did use both queries and test cases, but each for a different ontology), the results in both cases are highly significant (for $\alpha = 0.05$ and $\alpha = 0.0001$, respectively).}
port is beneficial in terms of the efficiency of the debugging process.

![Violin plots showing the distribution of the debugging task completion times in Study 2 for the query-based vs. the test case based approach.](image)

**Figure 6:** Violin plots showing the distribution of the debugging task completion times in *Study 2* for the query-based vs. the test case based approach.

![Violin plots showing the distribution of the number of user interactions to complete the debugging task in Study 2 for the query-based vs. the test case based approach.](image)

**Figure 7:** Violin plots showing the distribution of the number of user interactions to complete the debugging task in *Study 2* for the query-based vs. the test case based approach.

6.3.3. Additional Observations (Study 2)

*Users feel equally confident using both debugging approaches:* While again overconfident in general (cf. Section 5.3.3), the participants were approximately equally confident about having made no mistakes in the debugging process at all, both when using queries and test cases.\(^{22}\) Specifically, the average confidence in case of query assistance was 93\% and 92\% when using test cases.\(^{23}\)

*Intuitive focus on mere query answering:* Interestingly, without giving the participants who used the query-based debugger any instructions to do so, all of

\(^{22}\)Note that in Figure 4 some confidence values seem to be zero. However, in fact, these cases represent *unknown* confidence values where participants did not provide an answer to the question about their subjective belief in the correctness of their debugging result.

\(^{23}\)Standard deviation: 8\% (queries) and 17\% (test cases).
them continued answering queries until a single diagnosis was left (cf. Figure 4). Apparently, they therefore did not rely on the list of diagnoses when using the query-based approach. When relying on test case based debugging, in contrast, more than one quarter of the users selected their solution from a list of more than one diagnosis. In other words, at a certain point they stopped specifying further test cases and considered it more efficient to inspect the candidate list. We interpret this as a possible sign that test case based debugging was more tiring, and thus more demanding for the users than query answering.

Query answering is more efficient than test case specification: As both the query-based and the test case based approach result in the addition of a new test case per iteration\(^{24}\), we compared the time users needed per answered query and per specified test case, respectively. The result is very clear (cf. Figure 8). The average test case specification time (\(\approx 2:20\) min) was almost 60\% (and statistically significantly\(^{25}\)) higher than the average query answering time (\(\approx 1:30\) min).\(^{26}\) This shows that it is more efficient to classify pre-selected axioms as (non-)entailments than to think about specific axioms and classifying them. Overall, this result demonstrates the potential of query-based sequential diagnosis approaches to reduce debugging efforts.

Query optimization pays off: The average number of queries (11.6) that had to be answered until the true diagnosis was found by the users was lower than the average number of test cases (13.1) the users specified to isolate the true diagnosis.\(^{27}\) This shows that automatic (and optimized\(^{28}\)) test case selection tends to be more efficient than manual test case specification. In other words, the automated approach is better than users at selecting test cases that discriminate (well) between the candidates.

6.3.4. Existence of Oracle Errors (RQ3.2)

Both in Study 1 and Study 2, we observed that it is not uncommon that participants make errors when specifying test cases and when answering the system’s queries. While in either case the large majority of the inputs provided by the participants was correct, at least one mishap occurred to a considerable fraction of participants in both studies. Even in the main Study 2, where the participants were instructed more intensively and where the participants had a better formal education on ontology engineering, about one quarter of the participants made at least one mistake. In the context of the study, mistakes were made equally for the test case specification and the query answering tasks.

Our observations therefore point to a largely open issue in algorithmic testing and debugging approaches, which are usually based on the assumption that

\(^{24}\)In the query-based scenario the test case is selected by the debugger and classified (as positive or negative) by the user, whereas in the test case based scenario the test case itself and its classification is chosen by the user.

\(^{25}\)According to a Wilcoxon Rank-Sum Test with \(\alpha = 0.001\) (p-value = 8.96 \times 10^{-13}).

\(^{26}\)Standard deviation: \(\approx 1:30\) (queries) and \(\approx 2:50\) (test cases).

\(^{27}\)Standard deviation: 3.3 (queries) and 4.8 (test cases).

\(^{28}\)We used entropy-based query optimization as described in [25] in our study.
there are no oracle errors. Only a few works exist in the literature, which specifically address the problem of wrong user inputs, e.g., in the context of spreadsheet testing [92], Spectrum-based Fault Localization procedures [93], or general software testing [94].

Next, in Section 7, we will take first steps to address this largely open research question in the context of query-based knowledge base debugging. Specifically, we will describe an initial prediction model that allows us to estimate the probability of oracle errors depending on the complexity of the queries asked to the user.

7. Predicting Oracle Errors based on Query Complexity

When designing a query-based debugging method, different options are available with respect to what types of queries are asked to the users. A closer look at the wrong user inputs in Study 1 and Study 2 revealed that from the faulty test case specifications about two thirds had a non-trivial syntactic structure, involving, for example, complex class expressions with intersection, union, or complement operators, as defined in the OWL specification [70]. This supports the intuitive assumption that the syntactic complexity of the required inputs is correlated with the probability of a user error.

The goal of the work described in this section is to develop a first model that allows us to estimate the probability of user error for a given query. The model can then be used by designers of interactive debugging systems, for example, in order to vary the complexity of the queries depending on the assumed expertise of the user. Alternatively, the model can be used to provide additional hints to the user in case of complex queries.

The proposed model was developed and evaluated with the help of two additional studies, which were performed in the context of Study 1 and Study 2. The first of these studies, termed Study E1, aimed at (i) verifying the conjecture that an axiom’s syntactic complexity has indeed a significant impact on how well it is understood and (ii) collecting data as a basis for the design of the
prediction model. The second study, termed Study E2, was conducted to assess the utility of the model.

7.1. Collecting Data for the Prediction Model (Study E1)

We designed a pen-and-paper study, where the task of the participants—the same ones as in Study 1—was to determine the correct translation of axioms written in OWL (Manchester Syntax [90]) into natural language and vice versa. Each participant was provided with ten axioms that were randomly chosen from a larger pool of manually-prepared axioms. The axioms themselves, which again related to the university and IT domain, were designed to have different complexity levels. A simple axiom, for example, would be \( X \text{ SubClassOf } Y \), where \( X \) and \( Y \) are class names from the respective domain. More sophisticated axioms involved complex class expressions such as \( \text{not}(X \text{ and } Y) \) or \( p \text{ some } (X \text{ or } Y) \) which use, e.g., property restrictions and different logical operators. An example of a more complex axiom would be \( \text{UndergradStudent SubClassOf not (hasDegree some Degree)} \).

For each given axiom, the participants were provided with three possible translations, where only one of them was correct. They then had to assign confidence scores to these answer options that express their degree of belief in the correctness of the respective answer.

To verify our hypothesis that syntactically more complex axioms are more difficult to comprehend, we proceeded as follows. First, we gathered the confidence scores the participants gave to the correct answers for all the translation tasks. Next, we asked two experts to classify the syntax patterns that occurred in the exercises as either particularly hard or particularly easy or neither. We then compared the recorded confidence scores between the group of hard and the group of easy syntax patterns. The average score was 0.55 for the former and 0.95 for the latter group. The statistical significance of this difference was revealed by a Wilcoxon Rank-Sum Test with level \( \alpha = 0.01 \) (p-value = 0.0015). That is, axioms of higher complexity indeed led to a lower success rate of the translation task. Overall, this finding supports the relevance of a syntax-based prediction model.

To obtain further insights regarding which syntactic features cause difficulties for the users, we manually inspected all answers of the participants. As a result, we identified the following major factors that increase the complexity for the participants: (a) nesting of class expressions, (b) negation in general, and (c) negated expressions that are not represented in “negation normal form” (NNF), i.e., which include negated complex class expressions.

7.2. Design of the Prediction Model

Based on the lessons learned from the different studies and on our researcher expertise, we constructed a rule-based prediction model, which takes a query in OWL as an input and returns a score that expresses how likely it is that the query will be properly understood. In other words, the model will tell us the likelihood of an oracle error for the given query.
The idea of the model is to recursively reduce a query to the axioms it consists of, and to then decompose these axioms to the class expressions they comprise. These expressions are in turn successively split into smaller sub-expressions, and so forth, until atomic classes are obtained. Based on the encountered syntactic structure, the model uses respective weights to compute the final query score when the recursion unwinds. The weights are defined based on the observations of our study.

For instance, the model assigns $X \text{SubClassOf} Y$ a score of 1 (maximum “easiness”) because such axioms were always correctly understood by the participants. In contrast, the score for $X \text{SubClassOf} \neg (p \text{some} Z)$ would be 0.25 due to the involved negation and property restriction. Note that the axiom $X \text{SubClassOf} p \text{only} (\neg Z)$ that expresses the same fact but is written differently in NNF would be indeed rated as being easier (score 0.29) by the model, which is in accordance with our observations.

To initially validate our model, we performed a correlation analysis based on Study E1. The analysis revealed that the predictions for the exercises from Study E1 are well in line with the success rates we had observed in the study ($\text{Pearson's } r = 0.53$). For the sake of brevity, we only sketched the main idea of the model here. The exact definition of the model can be found in Appendix A.

7.3. Evaluation of the Prediction Model (Study E2)

Study E2, which involved the participants of Study 2, was a pen-and-paper exercise that we conducted to validate the predictive power of our model directly, i.e., through a query answering task. In the study, each participant was provided with a natural language description of a university domain and 25 queries in OWL Manchester Syntax, each consisting of one axiom. The queries were randomly selected from a pool of logical axioms $ax_i$ involving 51 syntactic patterns of different complexities, with scores predicted by our model ranging from 0.05 (hard) to 1 (easy). For each query, the task was to decide if it is true or false in the given domain. The correct answers to all 25 questions were given in the natural language text, i.e., the participants did not have to make any assumptions to correctly answer the queries. The participants were again asked to provide, for each query, on a scale from 0 to 100, (i) a difficulty assessment and (ii) their confidence in the given answer.

From the subjects’ questionnaires, we extracted, grouped by syntactic pattern, (a) the percentage of correct answers, (b) the users' average confidence in their answer, and (c) the average subjective difficulty. A comparison of each of these three response variables with the model predictions yielded quite decent correlation coefficients of 0.36, 0.52, -0.70 for (a), (b) and (c), respectively. Moreover, to assess the statistical significance of the model’s predictive power, we ranked all queries according to their score as per our prediction model and performed a median split of the axioms into two groups, one including the easy and one the hard syntactic patterns. An analysis of the response variables (a), (b) and (c) for these two groups revealed that there is a significant between-group difference (Wilcoxon Rank-Sum Test, p-values $< 10^{-5}$, $< 10^{-5}$.
and 0.0197) which confirms the predictive power of the proposed model. As a result, axioms that were estimated to be hard according to the model (i) in fact led to a higher failure rate, (ii) were actually perceived to be harder, and (iii) resulted in a lower confidence of the users in their answers. The same relationship holds in the other direction.

As a side note, the prediction model, in case it did not exactly predict the observed success rate, tended to underestimate the success probability. As a consequence, whenever the model predicted that a query is easy (i.e., had a score close to 1), it actually proved to be very well understood by the users. Hence, using methods in a query-based debugger that are able to generate “easy questions” with respect to such a prediction model is expected to be beneficial to avoid oracle errors. Examples of such methods can be found in [53, 85, 79].

7.4. Discussion

Overall, our results indicate that our model, although still preliminary, is able to assess the complexity of a given query with good reliability. Clearly, more research is required to further develop the model and to validate it for other problem settings. Nonetheless, we see the results as an important first step in the direction, which can be used when designing an interactive debugging environment.

Furthermore, the model can also be used for other purposes related to debugging, e.g., as an estimator of the prior fault information provided to a debugger. For instance, a higher fault probability could be assigned to axioms in the KB that are rated as hard by the prediction model. As pointed out and empirically proven by several works [81, 25, 82], reliable fault probabilities are a crucial ingredient to efficient fault localization but are often difficult to estimate.

8. Research Limitations

Our research does not come without limitations. First, the number of participants in the different studies, while being larger than in some previous studies on the topic, could be higher, and we plan to conduct additional experiments in the future with a larger set of participants. The participants of our studies were computer science students and all had a comparable background. We argue that this participant group is representative of at least a part of the population of real-world knowledge engineers, i.e., those that have a formal education in computer science.

The experiments conducted in Study 1 and Study 2 are each based on two specific knowledge bases (ontologies). While we thereby tried to make sure that the insights are not limited to one single domain, our experiments were based on ontologies with a comparable level of complexity. To what extent our insights generalize to much larger or more complex knowledge bases, can therefore not be concluded with certainty from the made experiments. However, in the light of the following considerations it seems plausible to expect that the obtained results regarding debugging efficiency carry over to harder debugging problems as well.
First, we used ontologies, which are already highly expressive (SROIQ) in Description Logic terms and hence simulate scenarios where users are confronted with very complex problems from the comprehension and reasoning point of view. Second, we observed that users required (i) significantly (almost 40\%) less time per query than per test case, and (ii) a comparable but by tendency smaller number of queries than test cases per debugging session. This suggests growing (absolute) time savings of the query-based over the test case based approach when larger debugging problems involving more fault candidates and more user interactions are considered.

The prediction model presented in Section 7 is still preliminary and must be seen more as a general indicator than a precise, optimized predictor. In fact, the scores that describe the complexity of an axiom are, for now, estimates that are based on a single study and on our own researcher expertise. However, our model evaluation clearly indicates that the rules, i.e., the way of using the structure of an axiom for the estimation (e.g., deeper nesting of sub-clauses is harder), are plausible.

9. Summary

Tool support for debugging is not only relevant for traditional software systems, but also for knowledge-based systems. In the field of general software engineering, more and more research works are published which aim at better understanding the true value of such debugging tools for developers. In the field of knowledge-based systems, research on this topic is however still limited. With this work, we aim to contribute new insights regarding the usefulness of query-based knowledge base debugging in contrast to a more traditional test case based approach.

We conducted different user studies to address some of the open questions. The studies showed that users who were supported by any of the two forms of a model-based debugger were able to successfully locate a large fraction—in one study almost all—of the faults in the given knowledge bases. This emphasizes the usefulness of model-based knowledge debugging in general. The query-based approach furthermore proved to be advantageous in terms of the efficiency and, thus, the required user effort in the debugging process. Users not only needed less time and fewer mouse clicks to locate the faults, the internal, optimizing query selection strategy also reduces the number of test cases that are needed to isolate the true cause of the observed problems.

Finally, the studies revealed certain other phenomena of knowledge base debugging processes. One main insight is that measuring the capability of a debugging method to properly rank the fault candidates should not be the only measure to compare different strategies. Another important aspect is that users sometimes provide wrong inputs to the debugging process. Future debuggers should therefore be able to take this aspect into account. In this work, we made a first step in this direction and proposed and evaluated a model that predicts the reliability of the user input for a query of a given complexity. Such
predictions can, for example, be used in future systems to decide on which types of queries should be asked to the user in query-based approaches.

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Appendix A. Formal Characterization of the Complexity Prediction Model

The suggested prediction model for query complexity is a function $M$ that maps a query $Q$—consisting of a set of OWL\textsuperscript{29} axioms\textsuperscript{30}—to a real-valued score in $(0, 1]$ where 1 means maximally easy and 0 maximally hard, respectively. Intuitively, $M(Q)$ can be interpreted as an estimate of the query’s probability to be comprehended properly by a user.

The assumption behind the model is that different expressions (logical operators, quantifiers, etc.) appearing in axioms have different complexities. To describe these complexities, we use a set of weights that are chosen empirically and based on our expertise. These weights are incorporated into a set of manually defined recursive rules. We use these rules to derive the complexity of a given query by decomposing it stepwise to its smallest components.

Computationally, the underlying idea of the model is to first extract from the query the axioms it consists of. Each of these axioms is then reduced to the class expressions it comprises. The class expressions are then recursively split into smaller sub-expressions until atomic classes are obtained. Based on the structure of the axiom found by this recursive reduction, the model uses the specified weights to compute the complexity of the axiom. Finally, the complexities of all query axioms are combined to compute the final query score.

In the following, we will describe in more detail (I) how axiom complexities are used to determine the overall query complexity, (II) how axiom complexities are derived based on the class expressions occurring in them, and (III) how complexities of class expressions are calculated.

The function $M$ makes use of two additional functions. The function $M_{ax}$ computes for a given OWL axiom its estimated probability in $(0, 1]$ of being understood correctly; $M_{ce}$ computes for a given OWL class expression its complexity in terms of a real number in $[1, \infty)$.

(I) Overall query complexity: Let $Q = \{ax_1, \ldots, ax_k\}$ be a query consisting of the OWL axioms $ax_i$, $i \in \{1, \ldots, k\}$. Then, we define

$$M(Q) := \prod_{i=1}^{k} M_{ax}(ax_i)$$

That is, the probability of $Q$ being answered correctly is equal to the probability of all axioms in $Q$ being answered correctly (assuming independence between the axioms).

(II) Axiom complexity: Let $ax$ be an OWL (class expression) axiom. An axiom $ax$ has one of the following forms [70] for some integer $s \geq 2$ and arbitrary OWL class expressions $X_1, \ldots, X_s$:

\textsuperscript{29}Whenever we write OWL in this section, we mean the OWL 2 Web Ontology Language, as specified in [70].

\textsuperscript{30}Currently, the model supports only class expression axioms. It can however be extended to cover object property, data property and assertion axioms as well.
We denote by \( CE(ax) \) the set of all class expressions occurring in \( ax \) and specify

\[
M_{ax}(ax) := \prod_{X_i \in CE(ax)} \frac{1}{M_{ce}(X_i)}
\]

That is, the probability of understanding the entire axiom is equal to the probability of properly comprehending all class expressions occurring in the axiom (assuming independence between the user’s understanding of the individual expressions). The estimated probability of comprehending a class expression is inversely proportional to the complexity of the expression, as assessed by \( M_{ce} \).

(III) Class expression complexity: 

We define \( M_{ce} \) recursively as follows. Let \( X_1, X_2, X_3, X_4, X_5, X_6 \) be (complex or atomic) OWL class expressions, \( A \) an atomic OWL class, and \( C_1, C_2 \) complex OWL class expressions. With an atomic OWL class we associate a named class, \( \top \), \( \bot \), or an enumeration of individuals. Further, let \( r_o \) be an OWL object property, \( r_d \) an OWL data property, \( r \) an OWL (data or object) property, \( R \) a data range, \( Q \in \{\forall, \exists\} \), \( N \in \{=, \leq, \geq\} \), as well as \( m \) a non-negative integer, \( v \) an individual and \( l \) a literal. Then:

\[
M_{ce}(A \sqcap C_1) = M_{ce}(C_1 \sqcap A) = M_{ce}(A) \cdot (1 + M_{ce}(C_1))
\]

if \( C_1 = X_3 \sqcup X_4 \)

\[
M_{ce}(C_1 \sqcap C_2) = (1 + M_{ce}(C_1)) \cdot (1 + M_{ce}(C_2))
\]

if \( C_1 = X_3 \sqcup X_4, C_2 = X_5 \sqcup X_6 \)

\[
M_{ce}(X_1 \sqcap X_2) = M_{ce}(X_1) \cdot M_{ce}(X_2)
\]

\[
M_{ce}(A \sqcup C_1) = M_{ce}(C_1 \sqcup A) = M_{ce}(A) \cdot (1 + M_{ce}(C_1))
\]

if \( C_1 = X_3 \sqcap X_4 \)

\[
M_{ce}(C_1 \sqcup C_2) = (1 + M_{ce}(C_1)) \cdot (1 + M_{ce}(C_2))
\]

if \( C_1 = X_3 \sqcap X_4, C_2 = X_5 \sqcup X_6 \)

\[
M_{ce}(X_1 \sqcup X_2) = M_{ce}(X_1) \cdot M_{ce}(X_2)
\]

\[
M_{ce}(Q r_o A) = M_{ce}(N m r_o A) = 1 + M_{ce}(A)
\]

\[
M_{ce}(Q r_o C_1) = M_{ce}(N m r_o C_1) = 2 \cdot M_{ce}(C_1)
\]

\[
M_{ce}(Q r_d R) = M_{ce}(N m r_d R) = M_{ce}(N m r) = 2
\]

\[\text{For brevity of notation we use Description Logic Syntax in the following description wherever possible. E.g., “\( \sqcap \)”, “\( \sqcup \)”, “\( \neg \)” stand for the OWL Manchester Syntax keywords and, or and not, respectively. For details see [90, Fig. 3].}\]

\[\text{OWL keyword ObjectOneOf [70].}\]
\[ M_{ce}(\text{ObjectHasValue } r v) = 2 \]
\[ M_{ce}(\text{ObjectHasSelf } r) = 2 \]
\[ M_{ce}(\text{DataHasValue } r l) = 2 \]
\[ M_{ce}(A) = 1 \]
\[ M_{ce}(\neg A) = 1.25 \]
\[ M_{ce}(\neg C_1) = 2 \cdot M_{ce}(C_1) \]

Importantly, each class expression \( ce \) is evaluated from top to bottom, i.e., the first of the above equations that is applicable is used to assess \( ce \).