The bearing capacity of footings on sand with a weak layer

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Minor details of the ground, such as thin weak layers, shear bands and slickensided surfaces, can substantially affect the behaviour of soil–footing and other geotechnical systems, despite their seeming insignificance. In this paper, the influence of the presence of a thin horizontal weak layer on the ultimate bearing capacity of a strip footing on dense sand is investigated by single-gravity tests on small-scale physical models of the soil–footing system. The test results show that the weak layer strongly influences both the failure mechanism and the ultimate bearing capacity if its depth is lower than about four times the footing width. It is found that the presence of a thin weak layer can cause decreases of the ultimate bearing capacity of up to 80%. Numerical simulations, by finite-element analysis, of the behaviour of the reduced-scale models are able to capture the failure mechanism and the ultimate bearing capacity correctly, only if the mean equivalent constant value of the secant angle of shearing resistance used in calculations is selected, taking into account the curvature of the shear strength envelope of the sand within the very low normal stress range existing in the tested models.

Notation

- **B** footing width
- **C_U** uniformity coefficient
- **c_0** cohesion intercept of sand
- **D_r** relative density
- **d** particle diameter
- **d_{10}** particle diameter corresponding to 10% of finer by weight
- **d_{50}** mean particle size
- **d_{60}** particle diameter corresponding to 60% of finer by weight
- **d_{max}** maximum particle size of sand
- **d_{min}** minimum particle size of sand
- **E'_y** Young’s modulus
- **e** void ratio
- **e_0** initial void ratio
- **e_{max}** maximum void ratio
- **e_{min}** minimum void ratio
- **G_s1** specific gravity of sand
- **K_o** coefficient of earth pressure at rest
- **L** footing length
- **l_m** lateral extent of failure mechanism
- **N_f** bearing capacity factor
- **n_0** initial porosity
- **n** porosity
- **Q** vertical load applied to the footing
- **q** mean vertical pressure acting on the footing base
- **q_{lim}** ultimate (or limit) bearing pressure (at peak) or ultimate bearing capacity
- **q_{lim,0}** ultimate bearing pressure (at peak) of footing on homogeneous sand bed
- **t_0** thickness of weak layer
- **z_1** depth from the ground surface of weak layer
- **z_m** depth from the ground surface of the deepest point of the failure mechanism
- **γ** unit weight of sand
- **γ_s1** dry weight of sand
- **γ_w** dry unit weight of weak layer
- **γ_s** specific unit weight of sand
- **β_f** angle of shearing resistance of the footing–sand interface
- **β_g** angle of friction of the glass–sand interface
- **η** ratio **q_{lim,0}/q_{lim,0}
- **θ** emersion angle of the failure surface: θ_l and θ_r on the left or right side of the footing, respectively
- **ν’** Poisson’s ratio
- **ρ** settlement of the footing
- **ρ_{lim}** settlement of the footing in correspondence of **q_{lim}
- **σ’** normal effective stress
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\( \sigma' \) \quad \text{vertical effective stress}  
\( \tau \) \quad \text{shear stress}  
\( \phi'_{1v} \) \quad \text{angle of shearing resistance of sand at constant volume}  
\( \phi'_{1p} \) \quad \text{peak angle of shearing resistance of sand}  
\( f'_{ip} \) \quad \text{mean equivalent constant value of secant angle of shearing resistance of sand}  
\( f'_{ip} \) \quad \text{angle of shearing resistance of the weak layer}  
\( \psi'_{ip} \) \quad \text{peak dilation angle of sand}  
\( \psi''_{ip} \) \quad \text{dilation angle corresponding to } \phi''_{ip}  

Introduction

Minor structural features can exist in natural soil and rock masses as well as in earthworks. They include thin syndigenic seams and laminae such as those occurring in varved soils, thin shear bands and sliding surfaces brought about by past instability processes, interfaces between different materials, structural discontinuities, contact surfaces (sometimes slickensided) between successive lifts in earth embankments. These ‘details’ may differ considerably from the adjoining materials in terms of index properties, shear strength, stiffness and hydraulic conductivity. Due to their thinness, they may pass undetected even when an ordinarily suitable ground investigation programme has been carried out. Terzaghi (1929) termed these features ‘minor geologic details’ and pointed out their enormous potential effects on the safety of dams; many subsequent studies (e.g. Rowe (1972, 1991), Leonards (1982), Scott (1987), Skempton and Vaughan (1993)) considerably added to the subject. The influence of minor geologic details of the ground on which the footing is founded does not appear, to the authors’ knowledge, to have been systematically investigated yet. The simplest of such details is exemplified by a thin horizontal soil layer weaker than the soil in which it is interposed. In the present paper, the results of an investigation into the influence of such a weak layer on the ultimate bearing capacity of strip footings on dense sand, by means of tests on reduced-scale physical models, are reported and discussed.

The problem is schematised in Figure 1. Plane strain conditions are considered. The strip footing is rigid and rests on the ground surface. The embedment depth is initially nil. The foundation soil consists of two materials: dry sand (variety A or B) and a thin layer, with thickness \( t_0 \), composed of a material weaker than the sand, located at depth \( z_0 \). The initial dry unit weight of the sand is \( \gamma_0 \). The peak angles of the shearing resistance of the sand and of the weak material are respectively \( \phi_{ip} \) and \( \phi''_{ip} \). Actually, the foundation soil consists of three layers (except when the weak layer is lacking) – namely, an upper and a lower sand layer plus the interposed weak layer. The load \( Q \) is vertical and centred. The sand is initially homogeneous in terms of its index properties; however, its shear strength parameters and stiffness in the physical model may not be constant within the relevant geotechnical volume of the foundation soil because of the curvature of the failure envelope in the range of very low stresses.

The main aim of the tests on reduced-scale models is to get a first insight into the effects of the weaker layer on the failure mechanisms and on the ultimate bearing capacity.

Experimental set-up and testing procedure

The experimental set-up is shown schematically in Figure 2. It consists of a parallelepipedal stiff box having the following outer dimensions: length: 1123 mm; width: 240 mm; height: 520 mm. The inside available space is 1000 mm long, 100 mm wide and 380 mm high. The front and rear walls of the box are made of poly(methyl methacrylate) (PMMA) plates, 25 mm thick, while the side walls are 20 mm thick. The bottom is also made of PMMA. The box rests on an 18 mm thick steel plate from which four vertical tee-steel sections stem at the corners; they are connected, in turn, to other horizontal steel sections in order completely to frame and stiffen the PMMA box. The lateral displacements of the front and rear walls can be considered negligible so that the plane strain (or two-dimensional (2D)) conditions apply. To reduce friction, the inside surfaces of the box are covered with a 2 mm thick glass sheet (see detail in Figure 2). The glass surface is coated with transparent silicone oil. The base of the box is tightly clamped onto the ram platen of a motorised hydraulic press. Other details of the apparatus are reported by Muscolino (2001).

The model footing is rigid; its width \( B \) is 40 or 60 mm, while its length \( L \) is 100 mm in both cases. At the top, the footing is connected to a vertical piston guided by an axial ball bushing so that the footing can move only vertically; the piston is connected, in turn, to a proving ring (or to a load cell) that reacts against the cross-head of the press. The footing is loaded by driving the box upwards by means of the press ram at a constant displacement rate of 0·6 mm/min.

The settlements of the footing are measured by a dial gauge. To reveal visually the displacements at different depths and the failure mechanism, initially horizontal rows of coloured sand particles are carefully placed in the sand layers and in contact with the glass sheet. To set a visual reference for displacements and distortions of the sand and the weak layer, a square grid of vertical and horizontal lines was carved on the external surface of the front PMMA wall. A digital camera was used to take pictures of the front wall in order to exploit the particle image velocimetry.
(PIV) technique for catching the evolution of soil displacements and the formation of the failure mechanism.

**Materials**

**Sands**
The soil layer consists of silica sand. Two sands, A and B, have been used. The sand grains are from subrounded to angular. The sands are essentially composed of silica (more than 95%) and traces of feldspars and calcite. The sand has been deposited by dry pluviation at a constant height of fall to achieve uniformity of the index properties within the sand. The target density was obtained by calibrating the height of fall and the size of the spreader hole. The height of fall of 1 m was kept constant during the deposition. Initial index properties of the sands are summarised in Table 1.
The relative density, $D_r$, was determined according to ASTM standards D 4253-00 and D 4254-00 (ASTM, 2004a, 2004b). Since the ratio $B/d_{50}$ is greater than 50 – specifically, 63·2 for $B = 60$ mm and 88·9 for $B = 40$ mm for footing on sands A and B, respectively – the particle size effect can be considered negligible according to recommendations made by many researchers (e.g. Bolton and Lau (1989), Taylor (1995), Toyosawa et al. (2013)).

The crushing of sand particles is negligible considering its mineralogical composition and the low stress level existing in the tested physical models (Valore and Ziccarelli, 2009).

The shear strength parameters of sands were determined by nine physical tests (Valore and Ziccarelli, 2009).

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The peak strength failure envelope of both sands is definitely curvilinear. The shear strength parameters of sand A vary in function of the normal stress level as shown in Figure 3. The angle of shearing resistance at constant volume, $\phi_{cv}$, obtained by means of triaxial tests and direct shear tests, is $34^\circ$. The shear strength parameters of sand B vary as follows: $c'_{1p} = 0$ and $\phi'_{1p} > 50^\circ$ for $\sigma'_e < 20$ kPa; $c'_{1p} = 0$ and $\phi'_{1p} = 50^\circ$ for $20 < \sigma'_e < 50$ kPa; $c'_{1p} = 0$ and $\phi'_{1p} = 45^\circ$ for $\sigma'_e > 50$ kPa; $\phi'_{av} = 32^\circ$.

These results are in good agreement with data reported in the literature (Celauro et al., 2014; Chakraborty and Salgado, 2010; Lancelot et al., 2006; Loukidis and Salgado, 2011; Negussey and Vaid, 1990; Ponce and Bell, 1971; Rowe, 1962; Sture et al., 1998; Yamaguchi et al., 1977).

The curvature of the failure envelope in the very low effective stress range is the most important single cause of the scale effects that afflict 1g tests on reduced-scale models; it cannot be neglected in the interpretation of the results of single-gravity physical tests (Hettler and Gudheus, 1988; Kumar and Khatri, 2008; Lau and Bolton, 2011a).

The angle of shearing strength for plane strain conditions is higher than the one obtained by triaxial tests due to the influence of the intermediate effective principal stress (Roscoe, 1970; Rowe, 1969; Sayão and Vaid, 1996). When $D_r$ is greater than 90% (relevant to the present research), the plane strain value of $\phi_{1p}$ may exceed the triaxial one by as much as 7° for values of the angle of shearing resistance at constant volume, $\phi'_{1cv}$, ranging from $30^\circ$ to $40^\circ$ (Abelev and Lade, 2004; Green and Bishop, 1969; Hoque and Tatsuoka, 1998; Lade and Duncan, 1973; Oda, 1981).

Materials making up the weak layer
Four materials have been used: three varieties of white dry talc powder $[\text{Mg}_3\text{Si}_4\text{O}_{10}(\text{OH})_2]$, namely, Baker, Luzenac 2 and CM3,
and bentonite (sodium (Na) montmorillonite) placed dry and then humidified by spraying distilled water. The peak angles of shear strength of these materials were determined by direct shear tests and are summarised in Table 2. The cohesion intercept and the strength of these materials were determined by direct shear tests, so the sand–footing contact can be considered perfectly rough according to Hansen and Christensen (1969) and Kumar and Kouzer (2007), since $\delta/\phi'_{p} > 0.7$ for $\phi'_{p} = 50^\circ$.

### Table 2. Angle of peak shear strength $\phi'_{p}$ of the weak layer

| Material                   | $\phi'_{p}$° |
|----------------------------|--------------|
| Dry Baker talc powder      | 31           |
| Dry Luzenac 2 talc powder  | 18           |
| Dry CM3 talc powder        | 27           |
| Humidified bentonite       | 11           |

### Glass–sand friction

The glass sheets have been lubricated with silicone oil. However, the interface is not perfectly smooth. The angle of friction $\delta_0$ of the sand–glass interface depends on the viscosity of the lubricating oil, the stress level, strain rate and smoothness of the glass surface (Goto et al., 1993; Tatsuoka et al., 1984). Tatsuoka and Haibara (1985) reported values of $\delta_0$ to be between 5° and 7° relative to the interface between Toyoura sand (which is a fine, essentially silica, sand) and non-lubricated acetone-cleaned glass.

Although in the experiments at hand the glass–sand friction is not nil, it is believed that the actual deformation state can be considered approximately 2D.

### Table 3. Sand A: results of $1g$ tests performed on physical models of strip footings resting on sand bed containing a thin horizontal weak layer

| Weak layer                  | Test | $z/B$ | $t_c/mm$ | $l_m/B$ | $z_m/mm$ | $d/m$ | $\theta_l/°$ | $\phi_k/°$ | $q_{lim}/kPa$ | $q_{lim}/q_{lim,0}$ | $\rho_{lim}/mm$ | $\rho_{lim}/B$ |
|-----------------------------|------|-------|----------|---------|----------|--------|-------------|-------------|----------------|----------------------|----------------|----------------|
| Dry Baker talc              | B05  | 1.47  | 2        | 2.50    | 88.2     | 0.95   | 40          | 36          | 307.9         | 0.82                 | 8.7            | 0.14           |
| B07                         | 0.50 | 2.5   | 4.75     | 105.5   | 1.75     | 32     | 34          | 41          | 318.8         | 0.99                 | 9.1             | 0.15           |
| B07                         | 0.95 | 3     | 2.50     | 57      | 0.95     | —      | 33          | 30          | 333.0         | 0.89                 | 8.8             | 0.15           |
| B09                         | 1.20 | 2.5   | 3.00     | 72      | 1.20     | 40     | 36          | 44          | 318.8         | 0.95                 | 9.0             | 0.15           |
| B10                         | 2.92 | 3     | 3.50     | 90      | 1.50     | 45     | 37          | 38          | 304.8         | 0.82                 | 9.2             | 0.15           |
| B11                         | 1.95 | 2.5   | 5.25     | 117     | 1.95     | 42     | 35          | 38          | 306.8         | 0.87                 | 8.7             | 0.15           |
| B12                         | 1.87 | 3     | 4.20     | 112.2   | 1.87     | 41     | 38          | 207.2       | 0.55           | 7.1                  | 0.12            |
| B13                         | 1.95 | 3     | 4.50     | 117     | 1.95     | 40     | 38          | 235.7       | 0.63           | 7.8                  | 0.13            |
| B14                         | 1.20 | 3     | 3.00     | 72      | 1.20     | 40     | 37          | 267.4       | 0.71           | 9.2                  | 0.15            |
| B15                         | 2.92 | 4     | 4.00     | 96      | 1.60     | 44     | 296.9       | 0.79        | 10.1          | 0.17                 |
| B21                         | 1.10 | 4     | 2.80     | 66      | 1.10     | 42     | 37          | 230.2       | 0.61           | 8.1                  | 0.13            |
| B22                         | 0.50 | 3     | 3.60     | 96      | 1.60     | 44     | 294.7       | 0.79        | 9.3           | 0.15                 |
| B33                         | 0.95 | 3     | 2.90     | 117     | 1.95     | —      | —           | 264.7       | 0.81           | 8.5                  | 0.14            |
| B42                         | 3.90 | 3     | 3.40     | 82.8    | 1.38     | —      | —           | 293.7       | 0.78           | 10.0                 | 0.17            |
| B49                         | 2.43 | 3     | 6.80     | 145.8   | 2.43     | —      | —           | 228.0       | 0.61           | 8.9                  | 0.15            |
| Humidified bentonite        | B16  | 1.20 | 3     | 3.00     | 72      | 1.20     | 33         | 37          | 117.6         | 0.31                 | 4.2             | 0.07           |
| B17                         | 1.92 | 4     | 3.50     | 115.2   | 1.92     | 42     | —           | 204.0       | 0.54           | 7.1                  | 0.12            |
| B18                         | 1.00 | 4     | 2.25     | 60      | 1.00     | 43     | 112.6       | 0.30        | 3.8           | 0.06                 |
| B23                         | 0.50 | 3     | 1.00     | 30      | 0.50     | —      | —           | 80.4        | 0.21           | 1.7                  | 0.03            |
| B37                         | 2.97 | 3     | 6.60     | 178.2   | 2.97     | —      | —           | 245.5       | 0.66           | 7.0                  | 0.12            |
| Homogeneous sand bed        | B06  | —    | 3.25     | 84      | 1.4     | —      | 41          | 375.1       | 1.0           | 8.29                 | 0.14            |

Results of test B06 on homogeneous sand bed reported for comparison $B = 60 mm,$ footing width; $z_c,$ depth of the top surface of the weak layer; $t_c,$ thickness of the weak layer; $q_{lim},$ ultimate bearing capacity; $q_{lim,0},$ ultimate bearing capacity for the homogeneous sand bed; $\rho_{lim},$ settlement of footing at limit pressure; $l_m,$ maximum lateral extent of failure mechanism; $\delta_0,$ maximum depth of failure mechanism; $\phi'_{p} = 375 \pm 1 kPa$, $\theta_l,$ and $\phi_k,$ emersion angles of the failure surface on the left or right side of the footing, respectively; other symbols defined in Notation.
Results of 1g tests on physical models
Fifty-four tests were performed in all (Muscolino, 2001), of which 45 were on sand A and 9 on sand B. Results of 18 of the tests performed on sand A are summarised in Table 3. Some tests were repeated at the same $z/B$ and are not listed in Table 3. Results of tests performed on sand B are summarised in Table 4. In Tables 3 and 4, the following data are given: the ultimate bearing capacity $q_{\text{lim}}$, the footing settlement $\rho_{\text{lim}}$ corresponding to $q_{\text{lim}}$, the depth and the material making up the weak layer, the main geometric characteristics of the failure mechanism.

The homogeneous dry sand bed test and the tests on dry sand containing a weak layer made of dry talc powder were, of course, drained. The tests involving a weak layer made of humidified bentonite can also be considered drained on account of the rather low displacement rate imposed on the footing, of the small thickness of the bentonite layer and of the dryness and high draining capacity of the sand bounding it.

Failure mechanisms
Typical failure mechanisms are shown in Figures 4–7 for $B = 60$ mm footing on sand A and in Figure 8 for $B = 40$ mm footing on sand B. The displacement fields and failure mechanisms relative to tests carried out on footing resting on sand A obtained by PIV analysis (Liu and Iskander, 2010; McMahon and Bolton, 2011; White et al., 2003) are reported in Figures 9–11. General shear failure (Vesic, 1973) occurred in all the experiments. The development of the failure surface started from the edges of the footing and then propagated downwards and laterally outwards, accompanied by the heaving of the ground surface on both sides of the footing. The complete formation of the failure mechanism during the loading process was clearly observed visually only after the peak load and was revealed by a shear band of dilated sand and by distortions undergone by the coloured sand rows (see Figures 4 and 5). This was observed through the front and rear walls of the testing box. The thickness of the observed shear band ranges from 6·1 to 9·1 mm corresponding to (6·3–9·1)$d_{50}$ for footings on sand A and from 3·2 to 5·4 mm corresponding to (7·1–12)$d_{50}$ for footings on sand B. In both cases, it is well within the range of (6–25)$d_{50}$ reported in geotechnical literature (Alshibli and Hasan, 2008; Finno et al., 1997; Mühlausen and Vardoulakis, 1987; Tatsuoka, 2001; Tatsuoka et al., 1991).

In the case of the homogeneous sand bed, the failure surfaces resemble that of Prandtl (1920), but their lateral extent is smaller (see Figures 4 and 8(a)); moreover, the angle of emersion at the ground surface $\theta$ is close to $45^\circ - \psi_{fp}/2$ instead of $45^\circ - \phi_f/2$, as found by Arens (1975).

The angles $\theta_0$ or $\theta_k$, reported in Tables 3 and 4, differ from $45^\circ - \psi_{fp}/2$ due to the dilation of the sand and range from 32 to 45° for footings on sand A and from 33 to 38° for footings on sand B; they approximately correspond to $45^\circ - \psi_{fp}/2$.

If the depth of the weak layer does not exceed a critical value (about 4$B$), it strongly influences both the failure mechanism and the ultimate bearing capacity, $q_{\text{lim}}$. The failure mechanism can cut across the weak layer when it is made of talc and is located at a depth $z_m$ of footings $z_m / B = 2$ instead of $45^\circ - \phi_f/2$.

![Figure 4. Homogeneous sand A bed. Failure mechanism observed in test B06. Thin lines are monogranular rows of blue-coloured sand particles adjacent to the box wall; they were initially horizontally aligned](image)

Table 4. Sand B: results of 1g tests performed on physical models of strip footings resting on sand bed containing a thin horizontal weak layer

| Weak layer          | Test | $z/B$ | $t_0$: mm | $l_{50}/B$ | $z_m$ : mm | $z_{nc}$ : mm | $\alpha_l$: ° | $\alpha_t$: ° | $q_{\text{lim}}$: kPa | $q_{\text{lim}}/q_{\text{lim,0}}$ | $\rho_{\text{lim}}$: mm | $\rho_{\text{lim}}/B$ |
|---------------------|------|-------|-----------|------------|-------------|--------------|---------------|---------------|-------------------|------------------------|----------------|-------------|
| Dry CM3 talc powder | B62  | 1·5   | 4·30      | 60         | 1·50        | 34           | 34            | 114           | 0·54              | 4·97                   | 0·08            |
|                     | B63  | 2·0   | 6·45      | 80         | 2·00        | 36           | 34            | 118           | 0·56              | 4·86                   | 0·08            |
|                     | B65  | 1·0   | 2·73      | 40         | 1·00        | 33           | 33            | 125           | 0·59              | 6·33                   | 0·11            |
|                     | B64  | 3·0   | 4·47      | 94         | 2·35        | 34           | 34            | 142           | 0·67              | 5·36                   | 0·13            |
|                     | B66  | 4·0   | 6·68      | 134        | 3·35        | 37           | 190           | 0·90          | 6·44               | 0·11                   |
|                     | B67  | 0·5   | 6·40      | 143        | 3·58        | 38           | 146           | 0·69          | 6·23               | 0·10                   |
| Homogeneous sand bed| B59  | —     | 4·85      | 107        | 2·67        | 33           | 211           | 3·45          | 0·07               |
|                     | B60  | —     | 6·10      | 135        | 3·38        | 34           | 212           | 5·08          | 0·08               |
|                     | B61  | —     | 4·10      | 110        | 2·75        | 36           | 196           | 4·21          | 0·07               |

Results of tests B59, B60 and B61 on homogeneous sand bed reported for comparison $B = 40$ mm, width of footing; $z$: depth of the top surface of the weak layer; $t_0 = 5$ mm, thickness of the weak layer; $q_{\text{lim}}$: ultimate bearing capacity; $q_{\text{lim,0}}$: ultimate bearing capacity for the homogeneous sand case, $\rho_{\text{lim}}$: settlement of footing in correspondence of ultimate bearing capacity; $l_{50}$: maximum lateral extent of failure mechanism; $z_m$: maximum depth of failure mechanism; $q_{\text{lim,0}} = 212$ kPa; $\theta_0$ and $\theta_k$: emersion angles of the failure surface on the left or right side of the footing, respectively; other symbols defined in Notation.
small depth underneath the footing; see Figures 5(a) and 6(a). The
failure mechanism usually develops in part along the weak layer
(see Figures 5(b), 6(b), 6(c) and 7).

The ratio $\rho_{\text{wil}}/B$ is almost constant for the weak layer made of talc
powder and ranges from 0·14 to 0·15 for the Baker talc, from
0·12 to 0·17 for the Luzenac 2 talc and from 0·08 to 0·13 for the
CM3 talc. For the weak layer made of humidified bentonite, the
$\rho_{\text{wil}}/B$ ranges between 0·03 and 0·12.

The relationship between the normalised lateral extent of the
failure mechanisms ($l_{\text{m}}/B$) and the depth of the weak layer ($z_{i}/B$)
is shown in Figure 12 for footings on sand A. The weak layer
clearly influences $l_{\text{m}}$ that becomes about twice as much as that for
the homogeneous sand case for $z_{i}/B$ ranging from 2·5 to 2·9. The
ratio $l_{\text{wil}}/B$ abruptly reduces when $z_{i}/B$ is about 3. For $z_{i}/B > 3$, the
values of $l_{\text{wil}}/B$ are about the same as that observed for the
homogeneous sand bed, irrespective of the material used for
the weak layer. For values of $z_{i}/B$ of about 0·5–0·6, $l_{\text{wil}}/B$ strongly
depends on the shearing resistance of the weak layer; when the
weak layer is made of humidified bentonite, $l_{\text{wil}}$ is very small,
while when it is made of talc powder (both Baker and Luzenac 2),
$l_{\text{wil}}$ is higher than that of the homogeneous sand bed. The
data in Table 3 show that the relation between $l_{\text{wil}}/B$ and the
maximum depth ($z_{\text{m}}/B$) of the failure mechanism is approximately
linear. The lateral extent of failure mechanism $l_{\text{wil}}$ is shorter than

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**Figure 5.** Sand A. Effect of the depth $z_{i}$ of the weak layer on the
failure mechanisms observed in tests (a) B07, (b) B08 and (c) B10.
Weak layer made of dry Baker talc powder, shown by double bold
lines. Other lines: monogranular coloured sand particles

**Figure 6.** Sand A. Effect of the depth $z_{i}$ of the weak layer on the
failure mechanisms observed in tests (a) B22, (b) B21 and (c) B49.
Weak layer made of dry Luzenac 2 talc powder, shown by double bold
lines.
that for the homogeneous sand bed ($l_{in} = 3·25B$) if the depth of the weak layer $z_i$ is smaller than the footing width $B$, while it is larger when $z_i$ exceeds $B$.

**Bearing pressure–settlement curves**

Typical vertical pressure ($q$)–settlement ($\rho$) curves are shown in Figures 13 and 14 for footing on sands A and B, respectively. They refer to a sand bed containing a thin weak layer made of humidified bentonite (test B16) or of dry Luzenac 2 talc powder (test B21). In both cases, the weak layer is located at a depth $z_i$ slightly larger than the footing width $B$. The experimental results of tests B06 and B60 relative to the homogeneous sand beds A and B are also plotted in the figures. The three curves are all characterised by a distinct peak corresponding to the ultimate bearing capacity, $q_{lim}$. Beyond the peak, $q$ undergoes a conspicuous, but not abrupt, decrease. For tests on sand A, the settlement in the correspondence of the peak $\rho_{lim}$ varies from 8·3 mm (when the weak layer is missing; test B06) to 8·1 mm (test B21) and to 4·2 mm (test B16), while for tests on sand B, $\rho_{lim}$ ranges from 5·1 mm (in the absence of the weak layer; test B60) to 6·2 mm (test B67) and to 5 mm (test B62). For tests on sand A, the presence of the weak layer causes $q_{lim}$ to reduce by 39% (from 375·1 to 230·2 kPa) and by 61% (from 375·1 to 117·6 kPa) for tests B21 and B16, respectively; for tests on sand B, $q_{lim}$ reduces by 41% (from 212 to 146 kPa) and by 46% (from 212 to 114 kPa) for tests B67 and B62, respectively. The regular post-peak behaviour is determined by the gradual reduction of the dilatation angle of the sand and by the increase of the depth below the ground surface of the footing base and, of course, by the imposed constancy of the settlement rate.

Before approaching the peak, the ‘stiffness’ of the soil–footing system, as measured by $\Delta\rho/\Delta\rho$, in the presence of the weak layer is smaller than the one corresponding to the homogeneous case (Figures 13 and 14), for footings resting on both sands A and B.

**Influence of the weak layer on the ultimate bearing capacity $q_{lim}$**

The ultimate bearing capacity, $q_{lim}$, has been normalised with respect to the ultimate bearing capacity relative to the sand bed without the weak layer, $q_{lim,0}$. The ultimate bearing pressure (at peak) of footings on a homogeneous sand bed, $q_{lim,0}$, is 375·1 kPa (for $B = 60$ mm) and 212 kPa (for $B = 40$ mm) for footings on sands A and B, respectively. The ratio $\eta = q_{lim}/q_{lim,0}$ is plotted against $z_i/B$ in Figure 15.

Each set of experimental results referring to weak layers made of the same material can be interpolated by a curve showing an upwards concavity and a well-defined minimum value of $\eta$. The curve relative to the weak layers made of Baker talc powder, characterised by an angle of shear strength $\phi_{ed} = 31^\circ$, shows a minimum at $z_i/B = 2·2$, at which the reduction in the ultimate bearing capacity, compared to the homogeneous sand case, amounts to 21·5%. The ultimate (or limit) bearing pressure (at peak) or ultimate bearing capacity, $q_{lim}$, tends to $q_{lim,0}$ (i.e. $\eta = 1$) for $z_i/B$ higher than 4. The curve relative to the weak layers made of Luzenac 2 talc powder ($\phi_{ed} = 18^\circ$) attains its minimum at $z_i/B = 1·9$, with a remarkable decrease in $\eta$ of 40·5% (from $q_{lim,0} = 375·1$ kPa to $q_{lim} = 223·2$ kPa). The ultimate (or limit) bearing pressure (at peak) or ultimate bearing capacity, $q_{lim}$, tends to $q_{lim,0}$ for $z_i/B$ larger than 4·3. The most dramatic reduction in $q_{lim}$ occurs when the weak layer is made of humidified bentonite ($\phi_{ed} = 11^\circ$); in this case, the minimum value of the interpolating curve was not precisely identified, but occurs at a value of $z_i/B$ lower than 0·5. The interpolating curve is poorly defined within the interval of $z_i/B$ from 0 to 0·5, in which $q_{lim}$ rapidly drops down. The maximum reduction in $q_{lim}$ amounts to 80%; $q_{lim}$ tends to $q_{lim,0}$ for $z_i/B$ values larger than 4·5.
Results of tests carried out on sand B (weak layer made of CM3 talc powder with $\phi'_{2p} = 27^\circ$) show a minimum at $z_i/B = 1.7$, and the reduction in $q_{lim}$ compared to $q_{lim,0}$ amounts to 45%; $q_{lim}$ tends to $q_{lim,0}$ for $z_i/B$ larger than 4.

The above results clearly demonstrate the great importance of the presence of a weak layer on the ultimate bearing capacity, which can decrease by as much as 80%. However, there is a threshold depth beyond which the influence of the weak layer becomes negligible, as expected. This depth is related to the shear strength of the material making up the weak layer. The effect of the weak layer on $q_{lim}$ depends essentially on $z_i/B$ and $\tan \phi'_{2p}/\tan \phi_{2p}$.

The effects of the thin weak layer depend on the difference between the shear resistance and deformability parameters of the sand and those of the weak layer, as well as on the thickness and depth of the latter. These factors affect the failure mechanism, the ultimate bearing capacity and the settlements of the footing; they cannot be considered as separable variables. In any case, the reduction of the ultimate bearing capacity and the modification of the failure mechanism induced by the presence of the weak layer derive fundamentally from the limited capability of the weak layer to transfer shear stresses to the underlying sand; clearly, the lower the shear strength of the weak layer, the stronger its influence.

For footings on homogeneous sand, the ultimate bearing capacity factor $N_j = 2q_{lim}(B)$ is equal to 781.5 and 670.9 for footings on sands A and B, respectively. These values are in very good agreement with the values reported in the literature for dense sands (Cerato and Lutenegger, 2007 (Figure 16(b)); de Beer, 1963, 1965; Diaz-Segura, 2013; Meyerhof, 1951; Vesić, 1973 (Figure 16(a))). The sands used by Cerato and Lutenegger (2007) are as follows: the Winter sand, angular and well-graded, $d_{50} = 0.7$ mm, $d_{10} = 0.2$ mm, $C_U = 45$, $\gamma_d = 18.8$ kN/m$^3$, $D_r = 87%$ and $\phi_{cv} = 40^\circ$; the brown mortar sand, less angular and well-graded than Winter sand, $d_{50} = 0.6$ mm, $d_{10} = 0.3$ mm, $C_U = 21$, $\gamma_d = 15.9$ kN/m$^3$, $D_r = 70%$ and $\phi_{cv} = 38^\circ$.

**Back-analysis**

The numerical simulations were performed with reference to the reduced-scale physical model. The dilation angle of the sands, $\psi'_{1p}$,
was evaluated according to Bolton (1986) as
\[ \psi'_{tp} = 1.25 (\phi'_{tp} - \phi'_{cr}), \]
\[ \phi'_{cr} = 34^\circ \text{ for sand A and } 32^\circ \text{ for sand B} \]
being the angle of shearing resistance at constant volume (i.e. at critical porosity). In finite-element (FE) back-analyses, the angle of the shearing resistance of the weak layer was assumed to be known, constant and equal to the one determined by direct shear tests; the dilation angle was considered nil. The back-analysis aimed at the determination of the secant mean equivalent constant angle of shearing resistance of the sand.

The main aim of the analyses is to back-calculate by successive trials an operative equivalent mean secant value of both the angle of shearing resistance, \( \psi'_{tp} \), and the dilation angle, \( \psi'_{tp} \), of the sand in correspondence of the ultimate bearing capacity, \( q_{lim} \). The unit weight of the materials and the angle of shearing resistance of the weak layer were assumed to be known. The cohesion intercept is always considered negligible. Plane strain state and drained conditions are assumed. To avoid mesh-related dissymmetries, only half of the model was analysed. The reference scheme for FE analysis along with the boundary conditions is shown in Figure 17. The vertical load \( Q \) corresponds to an average bearing pressure \( q \) on the soil–footing interface. Actually, a uniform

Figure 9. Test B06: footing on homogeneous sand A. Evolution of the displacements field, obtained by PIV analysis, in function of the applied pressure \( q \) and corresponding settlement \( r \) of the footing. The ratios \( q/q_{lim} \) and \( \rho/\rho_{lim} \) are indicated. \( q_{lim} = 375.1 \text{kPa}; \rho_{lim} = 8.29 \text{mm}: \) settlement at ultimate bearing pressure \( q_{lim}; q: \) current applied vertical pressure. White dashed line: failure mechanism.

Figure 10. Test B21: footing on sand A containing a horizontal weak layer made of Luzenac 2 dry talc powder. Evolution of the displacements field, obtained by PIV analysis, in function of the applied pressure \( q \) and of the corresponding settlement \( \rho \) of the footing. The ratios \( q/q_{lim} \) and \( \rho/\rho_{lim} \) are indicated. \( q_{lim} = 230.2 \text{kPa}; \rho_{lim} = 8.1 \text{mm}: \) settlement at ultimate bearing pressure \( q_{lim}; q: \) current applied vertical pressure. White dashed line: failure mechanism.
vertical settlement of the footing base is imposed instead, so as to reproduce the real experimental procedure and accounting for the high stiffness of the footing and for the roughness of its base (Lee et al., 2013). The finite-element code Plaxis 2D (Plaxis, 2008) was used. For soils, the simple elastic–perfectly plastic Mohr–Coulomb constitutive model with non-associated flow rule has been adopted, similar to many researchers (Bolton and Lau, 1993; Hjiaj et al., 2005; Kumar and Khatri, 2011; Loukidis and Salgado, 2009; Potts, 2003; Yin et al., 2001). Geometric variations of the system were disregarded. The latter hypothesis and the assumption of perfect plasticity imply that pre-peak hardening, post-peak strain softening and spatial dependence of

Figure 11. Test B23: footing on sand A containing a horizontal weak layer made of humidified bentonite. Evolution of the displacements field, obtained by PIV analysis, in function of the applied pressure \( q \) and of the corresponding settlement \( \rho \) of the footing. The ratios \( q/q_{\text{lim}} \) and \( \rho/\rho_{\text{lim}} \) are indicated. \( q_{\text{lim}} = 80.4 \text{ kPa}; \rho_{\text{lim}} = 1.7 \text{ mm} \): settlement at ultimate bearing pressure \( q_{\text{lim}} \); \( q \): current applied vertical pressure. White dashed line: failure mechanism.

Figure 12. Relationship between the normalised lateral extent of the failure mechanism \( (l_m/B) \) and the depth of the weak layer \( (z/B) \), footing resting on sand A. Footing width: \( B = 60 \text{ mm} \).

Figure 13. Footing on sand A. Typical bearing vertical pressure–settlement curves. \( B = 60 \text{ mm} \). Test B16: weak layer made of humidified bentonite, \( z/B = 1.20 \). Test B21: weak layer made of Luzenac 2 talc powder, \( z/B = 1.10 \). Test B06: homogeneous silica sand, shown for comparison.

Figure 14. Footing on sand B. Typical vertical bearing pressure–settlement curves. \( B = 40 \text{ mm} \). Weak layer made of CM3 talc powder. Test B62: \( z/B = 1.5 \). Test B67: \( z/B = 0.5 \). Test B60: homogeneous silica sand, shown for comparison.
the angle of shear resistance, $\phi'$, on stress level have not been taken into account.

Possible small effects linked to the progressive failure phenomenon (Bishop, 1967) were not considered, according to the observations made by many researchers on the basis of large- and small-scale and centrifuge tests (Hettler and Gudheus, 1988; Lau and Bolton, 2011a; Muhs, 1965; Yamaguchi et al., 1976, 1977). Muhs (1965) detected progressive failure in large-scale tests (square footing, base area of the footing = 1 m$^2$) and observed that it depended on the deformation level before failure and on the settlements of the footing; he considered that it is significant only for large settlements. Yamaguchi et al. (1976) found a marked localisation of the shear strains, by using the X-ray technique, but this observation refers only to the post-peak phase. Hettler and Gudheus (1988) found that the shear band influences the load–displacement curve mainly after the peak, and hence, an analysis of progressive failure is not necessary for the determination of the peak load. Lau and Bolton (2011a) recently observed that no strong evidence of progressive failure has been found in their tests.

The bearing pressure–settlement curves are back-calculated only up to the peak. Actually, the angle of shearing strength depends...
on the effective stress level and, consequently, it varies within the relevant soil volume, from ‘low’ values in the soil beneath the footing (where the effective normal stresses are relatively ‘high’) to ‘high’ values within the passive zone where the stresses in tested physical models are extremely low (Lau and Bolton, 2011a, 2011b).

Homogeneous sand bed
The homogeneous sand bed–footing system was first back-analysed. Experimental and calculated results (tests B06 and B60 for footing on sands A and B, respectively) agree fairly well as far as the ultimate bearing pressure, \( q_{\text{lim},0} \), and the bearing pressure–settlement curve (up to \( q_{\text{lim},0} \)) are concerned; see Figures 18 and 19. The following parameters of the sand were used: Young’s modulus \( E_0 = 10^4 \text{kPa} \), Poisson’s ratio \( \nu = 0.15 \), angle of shear strength \( \phi'_{\text{lp}} = 52.3^\circ \) angle of dilation \( \psi'_{\text{lp}} = 22.9^\circ \) and \( K_0 = 0.4 \).

Sand bed with a weak layer
The numerical analysis, despite the adopted simplifying assumptions, allows one to find out the failure mechanisms which match the experimentally observed ones very well as shown – for example, in Figure 20. This latter is to be compared with the results of test B22 (footing on sand A; weak layer made of Luzenac 2 talc powder; Figure 6). The values of Young’s modulus, of Poisson’s ratio and of the dry unit weight, \( \gamma_d \), of the

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**Figure 17.** Reference scheme for FE analysis. \( Q \): vertical load applied to the footing

**Figure 18.** Footing on homogeneous sand A. Incremental shear strains at failure

**Figure 19.** Footing on homogeneous sand A. Load–settlement curves from Test B06

**Figure 20.** Incremental shear strains at failure for \( z/B = 0.5 \). Weak layer made of Luzenac 2 talc powder. Compare with test B22 (sand A; footing width \( B = 60 \text{ mm} \)).
weak layer have been assumed to be equal to that of the sand bed ($E' = 10^4$ kPa, $v' = 0.15$, $\gamma_{sat} = 16.1$ kN/m$^3$). Other parameters of the weak layer were as follows: Baker talc powder: $\phi_p' = 31^\circ$, $K_0 = 0.4$; Luzenac 2 talc powder: $\phi_p' = 18^\circ$, $K_0$: $1 - \sin\phi_p'$; humidified bentonite: $\phi_p' = 11^\circ$, $K_0$: $1 - \sin\phi_p'$; CM3 talc powder: $\phi_p' = 27^\circ$, $K_0 = 0.4$. The calculations were performed assuming for sand A the values of $\phi_p' = 52.3^\circ$ and $\psi_p' = 22.9^\circ$ retrieved from the analysis of test B06 on homogeneous sand A and $\phi_p' = 50^\circ$ and $\psi_p' = 22.5^\circ$ obtained from the back-analysis of test B60 on homogeneous sand B. In the case of test B22, in which the weak layer is located at $z_i = 0.5B$, the failure mechanism crosses the weak layer, develops through a radial shear zone inside the sand underlying the weak layer and then runs upwards along a plane, inclined by $31.3^\circ$, which crosses the weak layer again before emerging on the ground surface.

Results of computations performed assuming $\phi_p' = 52.3^\circ$ and $\psi_p' = 22.9^\circ$ for sand A and $\phi_p' = 50^\circ$ and $\psi_p' = 22.5^\circ$ for sand

Figure 21. Results of back-calculations, $q_{lim}/q_{lim,0}$ in function of $z_i/B$. The value of $\phi_p^{*}$ pertinent to each test is reported in Tables 5 (sand A) and 6 (sand B). Weak layer made of (a) Baker talc powder, (b) Luzenac 2 powder, (c) humidified bentonite and (d) CM3 talc powder

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the weak layer and of its mechanical properties. The operatives of the sand applies for all the experiments regardless of the depth of the secant mean equivalent operative values of data. The results summarised in Tables 5 and 6 clearly show that triangles in Figure 21 and, of course, agree with experimental Bolton corresponding values of the calculated q and are summarised in Tables 5 (sand A) and 6 (sand B); the Table 6. mean equivalent values of the operative peak angle of shearing resistance \( \phi_{1p}^{*} \) and dilation angle \( \psi_{1p}^{*} \) of sand; \( B = 60 \text{ mm} \)

| Material of weak layer | \( \phi_{1p}^{*} \) | \( \psi_{1p}^{*} \) |
|------------------------|-----------------|-----------------|
| Baker talc powder      | 56.9            | 28.6            |
| Luzenac 2 talc powder  | 62.6            | 35.8            |
| Humidified bentonite   | 60.5            | 33.1            |
|                        | 59.5            | 31.9            |
|                        | 56.4            | 28.0            |
|                        | 55.5            | 26.9            |
|                        | 53.5            | 24.4            |
|                        | 52.3            | 22.9            |

Mean secant equivalent values of the operative peak angle of shearing resistance \( \phi_{1p}^{*} \) and dilation angle \( \psi_{1p}^{*} \) of sand; \( B = 60 \text{ mm} \)

B are plotted as open triangles in Figure 21, along with the experimental results. It is evident from these figures that the back-calculated values of \( q_{\lim} \) and, hence, of \( q_{\lim}/q_{\lim,0} \) are definitely lower than the experimental ones. The reason for this discrepancy is hidden in the hypothesis that only one value of \( \phi_{1p}^{*} \) and \( \psi_{1p}^{*} \) of the sand applies for all the experiments regardless of the depth of the weak layer and of its mechanical properties. The operatives \( \phi_{1p}^{*} \) and \( \psi_{1p}^{*} \) necessary to match the experimental values of \( q_{\lim} \) and of \( q_{\lim}/q_{\lim,0} \) of each test have been found by trial and error and are summarised in Tables 5 (sand A) and 6 (sand B); the corresponding values of the calculated \( q_{\lim} \) are plotted as solid triangles in Figure 21 and, of course, agree with experimental data. The results summarised in Tables 5 and 6 clearly show that the secant mean equivalent operative values of \( \phi_{1p}^{*} \) depend on both the depth and the mechanical properties of the weak layer. It can be observed that \( \phi_{1p}^{*} \) and \( \psi_{1p}^{*} \) (\( \psi_{1p}^{*} \) being linked to \( \phi_{1p}^{*} \) by Bolton’s relation: \( \psi_{1p}^{*} = 1.25 (\phi_{1p}^{*} - \phi_{0}^{*}) \) are higher when the length of the failure surface running along the weak layer is larger and the depth of the weak layer is smaller. These results clearly highlight the considerable relevance of the curvature of the failure envelope of the sand at very low effective normal stresses.

In other words, the numerical modelling, even though performed using a very simple constitutive model for soils, allows for the understanding of the fundamental aspects of the influence of a weak layer on the behaviour of shallow strip footings. It is able to capture the shape of the failure mechanism and the reduction of the ultimate bearing capacity observed in 1g tests on reduced-scale models, provided that due allowance is made for the dependence of the equivalent mean shear strength parameters on the effective normal stress level and on the depth of the weak layer.

**Conclusions**

The influence of a horizontal thin weak soil layer inside a sand bed on the mechanical behaviour of a strip footing loaded to failure was investigated by means of single-gravity (1g) tests on small-scale physical models. From the test results, the following conclusions can be drawn.

The weak layer strongly influences both the failure mechanism and the ultimate bearing capacity, \( q_{\lim} \) if its depth does not exceed a critical value of about 4B (B being the footing width). The failure mechanism cuts through the weak layer when it is located at small depths, \( z_{2} \), beneath the footing except when its shear strength is very low; when the weak layer is located at larger depths, \( z_{2} \) (however smaller than 4B), it forces the failure mechanism to run partly along the horizontal weak layer before rising through the upper sand layer and emerging on the ground surface.

The ultimate bearing capacity, \( q_{\lim} \), is always lower than \( q_{\lim,0} \) (pertaining to the homogeneous sand bed). At a given depth of the weak layer, the decrease in \( q_{\lim} \) is higher the lower the angle of shearing strength of the weak layer. The experiments show that the reduction in \( q_{\lim} \) can reach 80% when the weak layer is made of humidified bentonite. Numerical simulations of the behaviour of the reduced-scale physical model tests by FE analysis (even though using the very simple constitutive Mohr–Coulomb model) satisfactorily captures the failure mechanism and the ultimate bearing capacity, provided that the strong dependency of the angle of the shearing resistance of the sand at the extremely low stress level existing in the physical model is properly taken into account. Moreover, back-calculations point out that the mean equivalent mobilised angle of shearing resistance of the sand significantly depends also on the properties and depth of the weak layer.

**Table 5. Results of back-calculations for footing resting on sand bed A**

| \( z_{1} \) mm | \( z/B \) | Baker talc powder |
|---------------|---------|-------------------|
| 30            | 0.50    | 55.0              |
| 60            | 1.00    | 60.8              |
| 75            | 1.25    | —                 |
| 90            | 1.50    | 57.5              |
| 120           | 2.00    | 57.0              |
| 150           | 2.50    | 56.4              |
| 180           | 3.00    | 56.8              |
| 240           | 4.00    | 52.3              |
| 255           | 4.25    | —                 |

| Material of weak layer | \( \phi_{1p}^{*} \) | \( \psi_{1p}^{*} \) |
|------------------------|-----------------|-----------------|
| Baker talc powder      | 26.3            | —               |
| Luzenac 2 talc powder  | 33.6            | —               |
| Humidified bentonite   | 31.1            | —               |

**Table 6. Results of back-analysis for footing resting on sand bed B**

| \( z_{1} \) mm | \( z/B \) | CM3 talc powder |
|---------------|---------|----------------|
| 20            | 0.5     | 50.1           |
| 40            | 1.0     | 56.5           |
| 60            | 1.5     | 55.0           |
| 80            | 2.0     | 50.0           |
| 120           | 3.0     | 50.0           |
| 160           | 4.0     | 50.0           |

| Material of weak layer | \( \phi_{1p}^{*} \) | \( \psi_{1p}^{*} \) |
|------------------------|-----------------|-----------------|
| CM3 talc powder        | 22.6            | —               |
| CM3 talc powder        | 30.6            | —               |
| CM3 talc powder        | 28.8            | —               |
| CM3 talc powder        | 22.5            | —               |
| CM3 talc powder        | 22.5            | —               |

Mean secant equivalent values of the operative peak angle of shearing resistance \( \phi_{1p}^{*} \) and dilation angle \( \psi_{1p}^{*} \) of sand; \( B = 40 \text{ mm} \)
Another evident implication of this study’s findings is that the geotechnical engineer should never overlook or disregard minor geologic details during site investigations.

It is well known that results of single-gravity experiments on small-scale physical models are not straightforwardly transposable to real problems due primarily to scale effects (Bolton and Lau, 1989; Cerato and Lutenegger, 2007; de Beer, 1963, 1965).

In order to investigate the scale effects concerning the problem at hand, centrifuge-enhanced gravity experiments have been carried out; their results are reported in a companion paper (Zicarelli et al., 2017).

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