Application of Fuzzy FoPID Controller for Energy Reshaping in Grid Connected PV Inverters for Electric Vehicles

M. Manjusha1*, T. S. Sivarani2 and Carol J. Jerusalin1

1Department of EEE, Mar Ephraem College of Engineering and Technology, Elavuvilai, Marthandam, 629171, India
2Department of EEE, Arunachala College of Engineering for Women, Manavilai, Vellichanthai, 629203, India
*Corresponding Author: M. Manjusha. Email: manjushaj6191@gmail.com
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Abstract: By utilizing Fuzzy based FOPID-controller, this work is designed via the energy reshaping concept for Grid connected Photovoltaic (PV) systems for electric vehicles and this PV module has its own inverter which is synchronised with the utility grid. In grid connected PV system, the mitigation plays an important role where the capacity of PV arrays increases it maintains power quality and it is necessary to comply with some requirements such as harmonic mitigation. Unless a maximum power point tracking (MPPT) algorithm is used, PV systems do not continuously produce their theoretical optimal power. Under various atmospheric conditions, MPPT is obtained by using Perturb and Observe (P&O) techniques. A storage function in terms of DC-link voltage and current, and q-axis current is created, by means of which physical characteristics are studied. Further the energy reshaping is done with the aid of the proposed Fuzzy Fractional Order PID (Fuzzy-FoPID) framework. The FOPID control parameters λ and μ are optimally tuned by Grey Wolf Optimization technique (GWO). The results obtained verify the advantages of using Fuzzy-FoPID control as compared to conventional PID (Proportional Integral Derivative) control and FoPID control. The injected reactive power into the grid and the efficiency of the proposed systems is studied by extensive simulations.

Keywords: Current controller; voltage regulator; grid connected inverter; electric vehicles; PID controller

1 Introduction

Among various types of renewable energy resources as per the abundance of renewable resources, simple installation of PV technologies, secure operation with low operating costs, PV schemes are getting enormous popularity [1].

Proportional resonant control have fulfilled steady-state efficiency, but any variation in the frequency of the grid can have adverse effects on its performance [2]. The most sophisticated controller for tracking repetitive periodic signals including sinusoidal waveforms is the repetitive controller. The design of the FLC (Fuzzy Logic Controller) is becoming easy, without in-depth knowledge of the system, for complex
and nonlinear process. The adaptive nature by the fuzzy system enhances the FO controller’s dynamic output, through which the controller will respond quickly to the variation of parameters, so that improved control efficiency with simple physical understanding can be achieved [3]. GWO technique is employed to tune the parameters of PID controller of doubly-fed induction generator-based wind turbine [4]. This paper adopts GWO, which modifies the hierarchy of wolf hunting by introduction of further roles of wolf to achieve a balance between exploration and exploitation, and control parameters can be optimized by this algorithm.

Shun-Cheung Wang et al. (2020) suggest a simple and efficient maximum power tracking method that combines simplified model-based state estimation (SMSE) with the adaptive alpha perturb-and-observe (P&O) method. Swati Singh et al. (2020) represented that review of optimization and modeling methodologies, as well as the interface mechanism of various renewable energy sources with various control designs such as the Fuzzy Controller, Fractional Order FPID (Fuzzy PID) Controller, and FOPID (Fractional Order PID) Controller. Majid Dehghani et al. (2021) presented that to achieve the full PowerPoint; a fuzzy logic controller (FLC) was optimized by a combination of particle swarm optimization (PSO) and genetic algorithm (GA).

Research Gap

As stated above, various control algorithms have been proposed to improve the efficiency and various energy reshaping [5] approaches have been used. But still there is a need for improvement in efficiency for use in practical applications, hence the research.

Contribution of the proposed research include

i. A novel energy reshaping approach using Fuzzy FOPID controller is proposed.
ii. The above strategy has been applied to a grid connected PV inverter.
iii. To obtain maximum solar energy from the PV array under various atmospheric conditions, MPPT technique is utilized.
iv. The efficiency of the proposed approach is studied extensively and compared with the existing approaches available in the literatures.

2 Proposed Energy Reshaping Scheme for Grid Connected PV System

The proposed system is based on a grid-connected PV inverter with MPPT technology and the following converter descriptions and Fig. 1 are provided below. The inverter input is a DC source voltage or a rectifier output. The output is connected to the grid to transfer power [6] to the grid through a low-pass filter.

2.1 Photovoltaic (PV) Array

With the interconnection of several PV modules a photovoltaic array is a simple serial and/or parallel. In general, the modules are initially connected in a serial [7] manner to obtain the required voltage, when constructing a PV array.

Mathematical modelling of PV panel: As irradiation is proportional to current, diode is connected in parallel with the current source in the recombination losses are represented. The equivalent circuit of a functional PV cell where the current is produced is shown in Fig. 2 and the V-I characteristics of the PV array in Fig. 3.

\[
I_m = I_{ph} - I_d \left[ \exp \left( \frac{q(V_{PV} + I_m R_s)}{bKT} \right) - 1 \right] - \left( \frac{V_{PV} + I_m R_s}{R_{sh}} \right)
\]  

\(q\)–electron charge, \(I_{ph}\)– photo electric current, \(n\) -No. of cells in series, \(T\) -Absolute temperature in Kelvin, \(I_m\) - the current of module, \(k\) -Boltzmann constant, \(N_s, N_p\) – PV cells in series & b parallel
\[ I_{PV} = N_p I_{ph} - N_p I_s \left( \exp \left( \frac{q}{A K T_c} \left( \frac{V_{dc}}{N_s} + \frac{R_s I_{PV}}{N_p} \right) \right) - 1 \right) \]  

Eq. (2) shows the relationship between the current and voltage output, where \( A \) is the p-n junction ideality factor, that ranges from 1 to 5 and \( k \), the Boltzman’s constant (1.3806* 10^{-23} J/K).
I_{PV} - cell’s photo current, I_r - Reverse saturation current of cell, T_c - Reference temperature of cell in K, q-electron charge in Cb, V_{dc} - PV output voltage.

The photo electric current as a function of the short circuit current is expressed as follows.

\[ I_{ph} = I_{sco} \left( \frac{G}{G_0} \right) (1 + \alpha (T - T_0)) \left( \frac{R_s + R_{sh}}{R_{sh}} \right) \]

where \( I_{sco} \) is the short circuit current at standard insolation \( G_0(1000\text{W/m}^2) \) and standard temperature \( T_0(251^\circ\text{C}) \), \( \alpha \) is the module’s temperature coefficient for the current.

### 2.2 MPPT Technique

To get the MPP effectively under time-varying atmosphere P & O method is used. Temperature and power of the PV array (voltage and current), accurate monitoring of the MPP [8] is an essential factor in the model of effective solar [9] array systems [10].

P & O method: Variation in power is considered the major factor for MPPT in this process. Here, the successful perturbation in the duty cycle is in the same direction to hit the MPP on the rise in power, and would be in the opposite direction, on the decrease in power.

### 2.3 DC Link Requirements

For the PV system in which a storage function associated DC-link current, DC-link voltage and q-axis current are constructed. Apply Kirchhoff’s current law, the dynamics [11] of the DC side is obtained as follows

\[ C \frac{dV_{dc}}{dt} = I_{pv} - I_{dc} = I_{pv} - \frac{e_d i_d + e_q i_q}{V_{dc}} \]

\( C \) - DC bus capacitance

The three-phase two-level PV inverter dynamics in d,q frame is given in the below equation

\[ v_d = e_d + R i_d + L \frac{d i_d}{dt} + \omega L i_q \]

\[ v_q = e_q + R i_q + L \frac{d i_d}{dt} - \omega L i_d \]

\( e_d, e_q, i_d, i_q, v_d \) and \( v_q \) - dq-axis components of grid voltage, grid current, and PV inverter output voltage

R & L – resistance & inductance, \( \omega \) -synchronous frequency of AC grid.

Assume the power loss in PV inverter switches are ignored, the power balance equation relating DC input and the AC output is given by

\[ e_d i_d + e_q i_q = V_{dc} I_{dc} \]

where \( V_{dc} \) and \( I_{dc} \) - PV inverter input current and voltage state vector

\[ x = (x_1 x_2 x_3)^T = (i_d i_q V_{dc})^T, \text{output } y = (y_1 y_2)^T = (i_q, V_{dc})^T \text{ and input } u = (u_1 u_2)^T = (v_d, v_q)^T. \]
The state equation of PV inverter as in Eq. (5) and Eq. (7) is given as,

\[
x = \begin{pmatrix} \frac{-R}{L} x_1 - \omega x_2 - \frac{e_d}{L} \\ \frac{R}{L} x_2 + \omega x_1 - \frac{e_q}{L} \\ \frac{I_{pv}}{C} - \frac{e_d x_1 + e_q x_2}{C x_3} \end{pmatrix} + \begin{pmatrix} \frac{1}{L} & 0 \\ 0 & \frac{1}{L} \\ 0 & 0 \end{pmatrix} u
\]  

(8)

The tracking error \( e = (e_1, e_2)^T - i_q - i_q^* \), \( V_{dc} - V_{dc}^* \).

The control input ‘u’ appears explicitly, as differentiate the tracking error \( e \)

\[
\begin{bmatrix} \dot{e}_1 \\ \dot{e}_2 \end{bmatrix} = \begin{bmatrix} f_1(x) \\ f_2(x) \end{bmatrix} + B(x) \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} - \begin{bmatrix} i_q^* \\ V_{dc}^* \end{bmatrix}
\]  

(9)

where,

\[
f_1(x) = \frac{-R}{L} x_1 - \omega x_2 - \frac{e_d}{L}
\]

(10)

\[
f_2(x) = \frac{I_{pv}}{C} - \frac{e_d \left( \frac{-R}{L} i_d - \omega i_q - \frac{e_d}{L} \right) + e_q \left( \frac{-R}{L} i_q + \omega i_d - \frac{e_q}{L} \right)}{CV_{dc}} - \frac{(e_d i_d + e_q i_q)}{C^2 V_{dc}^2} I_{pv} + \frac{(e_d i_d + e_q i_q)^2}{C^2 V_{dc}^3}
\]

(11)

With \( B(x) = \begin{bmatrix} 0 & \frac{e_d}{LC_{Vdc}} - \frac{1}{LC_{Vdc}} \end{bmatrix} \) system’s candidate storage function can be developed

\[
H(i_q, I_{dc}, V_{dc}) = \frac{1}{2} (i_q - i_q^*)^2 + \frac{1}{2} (V_{dc} - V_{dc}^*)^2 + \frac{1}{2} \left( \frac{I_{dc}}{C} - V_{dc}^* \right)^2
\]

(12)

The storage function \( H(i_q, I_{dc}, V_{dc}) \) is given as as the sum of heat produced by q-axis current \( i_q \), DC-link voltage \( V_{dc} \) and DC-link current \( I_{dc} \).

### 2.4 Grid Connected Inverter

The inverter connected to the grid transforms DC into AC suitable for injection into the grid, usually 120 V RMS at 60 Hz or 240 V RMS at 50 Hz. Inverters [12] connected to the grid are used between local electricity generators [13] and this three-phase grid-connected PV inverter [14] configuration is shown in Fig. 4.

![Diagram showing three-phase grid-connected PV inverter configuration](image)

**Figure 4:** Three-phase grid-connected PV inverter configuration

The ideal voltage source [15] is in series with the grid impedance \( Z_g \). The grid current is expressed in Eq. (13), with an output impedance \( Z_{inv} \), the grid-connected inverter is considered a current source \( I_c \) in parallel. \( Z_g(s) / Z_{inv}(s) \) gives the grid-connected system \( P_m \) since under the assumption that current source \( I_c \) and the voltage source \( U_s \) are independently stable.
\[ I_g(s) = I_{cr}(s) - \frac{U_s(s)}{Z\text{inv}(s)} \frac{1}{1 + Z_g(s)/Z\text{inv}(s)} \] (13)

\[ H(s) = \frac{1}{Z_g(s)/Z\text{inv}(s)} \] (14)

The relative stability is proved, as the Pm of \( Z_g(s)/Z\text{inv}(s) \) does not affect real Pm of the grid connected system although \( I_{cr} \) is stable and the mathematical model of grid-connected inverter control system is shown in Fig. 5.

**Figure 5:** Mathematical model of grid-connected inverter control System

Provided that, according to Fig. 6, the inner loop is a proportional regulator \( K_c \) and outer most loop is a proportional-integral (PI) regulator. The transition function [16] of the closed loop is

**Figure 6:** Simulink diagram of proposed Grid connected PV system
\[
G_{\text{closed}}(s) = \frac{I_g(s)}{I_{\text{ref}}(s)} = \frac{G_C(s)K_C(s)K_{PWM}}{L_1L_2Cs^3 + m_1s^2 + m_2s + m_3}
\]  
(15)

\[
m_1 = (L_1K_CK_{PWM} + L_1Z_g)C
\]  
(16)

\[
m_2 = L_1 + L_2 + Z_gCK_CK_{PWM}
\]  
(17)

\[
m_3 = G(s)K_CK_{PWM} + Z_g
\]  
(18)

Considering that \(U_s\) is a perturbation, then \(I_g(s)\) can be rearranged as

\[
I_g(s) = I_{\text{ref}}(s)G_{\text{closed}}(s)
\]  
(19)

In Eq. (19), \(Z_o(s)\) - sum of the inverter output impedance, \(Z_{\text{inv}}(s)\) - grid impedance \(Z_g(s)\). Moreover,

\[
Z_{\text{inv}} = \frac{L_1L_2Cs^3 + L_2CK_CK_{PWM}s^2 + (L_1 + L_2)s + G(s)K_CK_{PWM}}{L_1Cs^2 + CK_CK_{PWM}s + 1}
\]  
(20)

\[
H(s) = \frac{L_1L_2Cs^3 + L_2CK_CK_{PWM}s^2 + (L_1 + L_2)s + G(s)K_CK_{PWM}}{L_1L_2Cs^3 + m_1s^2 + m_2s + m_3}
\]  
(21)

The coefficients of \(m_1, m_2\) and \(m_3\) can be seen in Eq. (18). According to Eq. (13), it can be rearranged as

\[
I_g(s) = I_{\text{ref}}(s)G_{\text{closed}}(s)
\]  
(22)

Calculated by the new mathematical model, comparing Eq. (22) with Eq. (19), Eq. (22) can be calculated as follows:

\[
I_g(s) = I_{\text{ref}}(s)G_{\text{closed}}(s)H(s) - \frac{U_s(s)}{Z_0(s)}
\]  
(23)

And \(G_{\text{closed}}(s)\) is

\[
G_{\text{closed}}(s) = \frac{G(s)K_CK_{PWM}}{L_1L_2Cs^3 + CK_CK_{PWM}s^2 + n_1s + n_2}
\]  
(24)

\[
n_1 = L_1 + L_2, \quad n_2 = G(s)K_CK_{PWM}.
\]  
(25)

3 Control Techniques and Energy Reshaping

3.1 PI Controller

The double loop control mode is adopted by a control system. The outer loop is used to manage the dc link voltage \((V_{dc})\). The proportional integral (PI) controller is used to regulate the grid current and the dc-link voltage. The transfer function [17] of the PI controller looks like the following:

\[
K_p + \frac{K_i}{s} = \frac{K_p s + K_i}{s}
\]  
(26)

\(K_p = \) Proportional gain, \(K_i = \) Integral gain.
### 3.2 PID Controller

Proportional Control, the most important of these, calculates the extent of the difference between set point and process variable (known as error) and then makes sufficient proportional adjustments to the control variable to remove the error. The Control law for PID Controller [18] is

\[
U = K_P e(t) + K_d \frac{d}{dt} e(t) + K_I \int_0^t e(t) \, dt
\]  

where \( K_d \) is the derivative gain.

### 3.3 FoPID Controller

The fractional order controller (PID \((\lambda, \delta)\)) is the same as the traditional PID controller, but the only difference is the fractional derivative order \((\delta)\) and integral order \((\lambda)\). The FoPID controller transfer function [19] illustration is given by,

\[
G_c(s) = \frac{u(s)}{e(s)} = k_p + k_i s^{-\lambda} + k_d s^{\mu}
\]  

where \( G_c(s) \) is controller transfer function, \( e(s) \) – error, \( c(s) \) – output. The term \( \lambda \) and \( \mu \) are the fractional of integral [20] parts and derivative parts [21].

The time domain representation of FoPID controller is given in Fig. 9.

\[
u(t) = K_p e(t) + K_i D^{-\lambda} e(t) + K_d D^{\mu} e(t)
\]  

### 3.4 Proposed Fuzzy FOPID Controller

The Fuzzy controller computes the scaling factor from error inputs to refresh the gain parameters of FOPID controller in an advanced systematic way.

\[
k_p = k_p + \Delta k_p
\]

\[
k_i = k_i + \Delta k_i
\]

\[
k_D = k_D + \Delta k_D
\]

where \( k_p, k_i, \) and \( k_D \) - initial gains of FoPID and

\( \Delta k_p, \Delta k_i, \) and \( \Delta k_D \) - scaling factors obtained from FLC.

For input and output fuzzy, triangle membership functions are used by applying Mamdani type inferencing system.

\[
\Delta k_p = (k_{p,max} - k_{p,min})k_p + k_{p,min}, \quad \Delta k_i = \frac{k_p^2}{(\pi k_d)}
\]

\[
\Delta k_d = (k_{d,max} - k_{d,min})k_d + k_{d,min}
\]

### 3.5 Proposed Fuzzy Based FOPID Control and Energy Reshaping

In the proposed method, FOPID attempts to designate a closed-loop energy feature which is analogous to the contrast between the system energy and the energy given by the controller. As follows, the energy modification equation is
\[
H[x(t)] - H[x(0)] = \int_{0}^{t} u^{T}(s)y(s)ds - d(t)
\] (34)

where \( H(x) \) - storage function

From Eq. (12) the very first term of the storage function \( \frac{1}{2}(i_q - i_q^*)^2 \) describes the power factor regulation the last two terms of the storage function, \( \frac{1}{2}(V_{dc} - V_{dc}^*)^2 \) and \( \frac{1}{2}(I_{dc} - I_{dc}^*)^2 \) shows the transformation from solar energy to electric current. PV output power \( I_{pv} \) variations reflects the change of DC-link voltage \( V_{dc} \) and DC-link current \( I_{dc} \) based on DC-link relationship. Differentiable storage function \( H(i_q, V_{dc}, I_{dc}) \) is given by

\[
H(i_q, I_{dc}, V_{dc}) = (i_q - i_q^*)\left( -\frac{R}{L}i_q + \omega i_d - \frac{e_d}{L} + \frac{1}{L}u_2 - i_q^* \right) + \left( \frac{I_{dc}}{C} - V_{dc}^* \right)
\]

\[
\times \left[ V_{dc} - V_{dc}^* + \frac{I_{pv}}{C} - \frac{e_d}{L}i_d + \frac{e_d}{L} + e_q\left( -\frac{R}{L}i_q + \omega i_d - \frac{e_d}{L} \right) \right]
\]

\[
\frac{C V_{dc}}{C^2 V_{dc}^2} - \left( \frac{e_d i_d + e_q i_q}{C^2 V_{dc}} \right) I_{pv} + \left( \frac{e_d i_d + e_q i_q}{C^2 V_{dc}} \right)^2 - \frac{e_d}{L C V_{dc}} - u_1 - \frac{e_q}{L C V_{dc}} u_2 + V_{dc}^*
\] (35)

Design Fuzzy based FoPID control for system,

\[
u_1 = -\frac{L C V_{dc}}{e_d} \left[ V_{dc}^* - V_{dc} + \frac{e_q}{L C V_{dc}} u_2 - \frac{I_{pv}}{C} - \frac{e_d}{L}i_d + \frac{e_d}{L} + e_q\left( -\frac{R}{L}i_q + \omega i_d - \frac{e_d}{L} \right) \right]
\]

\[-\frac{\left( e_d i_d + e_q i_q \right)}{C^2 V_{dc}} - v_1 \]

\[
u_2 = L i_q^* - \omega L i_q + R i_q + e_q - v_2
\] (36)

The additional inputs \( v_1 \) and \( v_2 \) is designed in the fuzzy based FoPID control form, as follows

\[
v_1 = K_{P1}(V_{dc} - V_{dc}^*) + \frac{K_{I1}}{S^\mu_1}(V_{dc} - V_{dc}^*) + K_{D1}S^{\mu_1}(V_{dc} - V_{dc}^*)
\] (38)

\[
v_2 = K_{P2}(i_q - i_q^*) + \frac{K_{I2}}{S^\mu_2}(i_q - i_q^*) + K_{D2}S^{\mu_2}(i_q - i_q^*)
\] (39)

As PID control gains \( K_{P1}, K_{P2}, K_{I1}, K_{I2}, K_{D1}, K_{D2} \), fractional differentiator order \( \mu_1 \) and \( \mu_2 \), \( \lambda_1 \) and \( \lambda_2 \) are selected to achieve sufficient convergence of the tracking error.

3.6 Grey Wolf Optimization (GWO)

Grey wolf belongs to Canidae family. The pioneers also called as alpha are a male and female. The alpha is responsible for settling on decisions. The pack are directed by the decision taken by the alpha.

3.6.1 Steps to Find the Optimally Tuned Parameters of the Fuzzy Based FoPID Controller Using GWO Technique

In various design problems, GWO can fundamentally increase the global optimum and provide an efficient and viable instrument for controller tuning. Encircling behavior is demonstrated by the following equations,
\[ D = |CX_p - AX(t)| \]  
(40)

\[ X(t + 1) = X_p(t) - AD \]  
(41)

Hunting behaviour is described by following equations

\[ \bar{D}_\infty = |\bar{C}_1\bar{X}_\infty(t) - \bar{X}(t)| \]  
(42)

\[ \bar{D}_{\beta_1} = |\bar{C}_2\bar{X}_{\beta_1}(t) - \bar{X}(t)| \]  
(43)

\[ \bar{D}_{\beta_2} = |\bar{C}_2\bar{X}_{\beta_2}(t) - \bar{X}(t)| \]  
(44)

\[ \bar{D}_{\delta_1} = |\bar{C}_3\bar{X}_{\delta_1}(t) - \bar{X}(t)| \]  
(45)

\[ \bar{D}_{\delta_2} = |\bar{C}_3\bar{X}_{\delta_2}(t) - \bar{X}(t)| \]  
(46)

\[ \bar{D}_{\delta_3} = |\bar{C}_3\bar{X}_{\delta_3}(t) - \bar{X}(t)| \]  
(47)

\[ \bar{X}_1^\prime = \bar{X}_\infty(t) - A_1(\bar{D}_\infty) \]  
(48)

\[ \bar{X}_{21}^\prime = \bar{X}_{\beta_1}(t) - A_2(\bar{D}_{\beta_1}) \]  
(49)

\[ \bar{X}_{22}^\prime = \bar{X}_{\beta_2}(t) - A_2(\bar{D}_{\beta_2}) \]  
(50)

\[ \bar{X}_{31}^\prime = \bar{X}_{\delta_1}(t) - A_3(\bar{D}_{\delta_1}) \]  
(51)

\[ \bar{X}_{32}^\prime = \bar{X}_{\delta_2}(t) - A_3(\bar{D}_{\delta_2}) \]  
(52)

\[ \bar{X}_{33}^\prime = \bar{X}_{\delta_3}(t) - A_3(\bar{D}_{\delta_3}) \]  
(53)

\[ \bar{X}(t + 1) = \frac{\bar{X}_1^\prime + \bar{X}_{21}^\prime + \bar{X}_{33}^\prime}{3} \]  
(54)

where \( t \) indicates the current iteration, \( \bar{X}_\infty(t), \bar{X}_{\beta}(t), \bar{X}_{\delta}(t) \) are the position of the grey wolves, \( \alpha, \beta \) and \( \delta \) at \( t^{th} \) iteration, \( \bar{X}(t) \) presents the position of the grey wolf at \( t^{th} \) iteration, \( F_k \) and \( F_{k-1} \) represent the fitness value obtained at the \( k^{th} \) and \( (k-1)^{th} \) iteration respectively.

Pseudo code of the GWO algorithm is presented below,

- Step 1: Initialize grey wolf population size \( X^i (i = 1, 2, 3, \ldots, n) \)
- Step 2: Initialize the parameters \( a, A, \) and \( C \)
- Step 3: Calculate fitness values of each search agent
  - \( X\alpha \) is best search agent
  - \( X\beta \) is second-best search agent
  - \( X\delta \) is third best search agent
- Step 4: Determine \( \alpha, \beta \) and \( \delta_1 \)
- Step 5: Update Hunting and Scouting
  - Hunting Eq. (42) to Eq. (47)
  - Scouting Eq. (48) to Eq. (53)
• Step 6: Fitness calculation of all search agents
  The fitness value is measured at the kth and (k-1)th iteration, respectively as F_k and F_{k-1}.
• Step 7: Determine the \( \alpha \), \( \beta \) and \( \delta_1 \) based on the Fitness value
• Step 8: Update the position of the current search agent by equation
  \[
  \tilde{X}(t + 1) = \frac{X_1^t + X_2^t + X_3^t}{3}
  \]
• Step 9: Update the parameters \( a \), \( A \), and \( C \)
• Step 10: Calculate fitness of entire search agent \( F_k - F_{k-1} \leq \varepsilon \)
  Update the parameters \( X_\alpha \), \( X_\beta \), and \( X_\delta \)
  While \( k = k + 1 \); end; return \( X_\alpha \).

### 3.6.2 Optimal Parameter Tuning Using GWO Techniques

The Fuzzy based FoPID control parameters in Eq. (38) and Eq. (39) are optimally tuned based on three cases, solar irradiation variation, temperature variation, and power grid voltage drop.

\[
\begin{align*}
\text{Minimize } F(x) &= \sum_{\text{Three cases}} \int_0^T \left( |V_{dc} - V_{dc}^*| + |i_q - i_q^*| + \omega_1 |u_1| + \omega_2 |u_2| \right) dt \\
\text{Subject to } &
\begin{cases}
K_{PI1}^{min} \leq K_{PI1} \leq K_{PI1}^{max} \\
K_{PI2}^{min} \leq K_{PI2} \leq K_{PI2}^{max} \\
K_{DI}^{min} \leq K_{DI} \leq K_{DI}^{max} \\
\lambda_i^{min} \leq \lambda_i \leq \lambda_i^{max} \\
\mu_i^{min} \leq \mu_i \leq \mu_i^{max} \\
u_{i min} \leq u_i \leq u_{i max}
\end{cases}
\end{align*}
\]

where the weights are \( \omega_1 \) and \( \omega_2 \).

### 4 Simulation Results and Discussion

To improve the efficiency and robustness of PV power generation, proposed approach develops a specific model of grid-connected PV system by MATLAB/Simulink environment that accurately represents the system’s qualities. To figure the performance of proposed GWO based Meta heuristic MPPT algorithm, the performance was compared with PI controller, PID controller, FOPID controller and Fuzzy FoPID controller. The proposed Grid connected PV system Simulink chart is shown in Fig. 6 and Tab. 1 shows the parameters of PI, PID and FoPID controllers. Simulink graph of FOPID controller based current regulation is shown in Fig. 7 and Fig. 8 shows the simulink diagram of Fuzzy FoPI controller.

| Controller, Parameter | PI controller | PID controller | FoPID controller | Fuzzy FoPID controller |
|-----------------------|---------------|---------------|-----------------|----------------------|
| Irradiance (W/m²)     | 1000          | 1000          | 1000            | 1000                 |
| V_{dc, mean} (V)      | 490 V         | 549 V         | 510 V           | 600 V                |
| P_{dc, mean} (kW)     | 240 kW        | 150 kW        | 300 kW          | 350 kW               |
| I_g (A)               | 0.18A         | 0.33A         | 0.28A           | 0.28A                |
4.1 PI Controller

From the outcomes, we can see that the output voltage of the PV panel settles down at 2 KV while the current worth changes depending on the irradiation. The $I_d$ reference esteem 0.03p.u which is given as the input sign of PI controller is shown in Fig. 9 and the Fig. 10 shows output voltage and current utilizing PI controller. As the output power used PI controller is shown in Fig. 11.

Sun irradiance is rapidly ramped down from 1000 W/m² to 200 W/m². Due to the MPPT operation, the control system lessens the $V_{dc}$ reference to 464 V to extricate maximum power from the PV cluster (46 kW). At $t = 0.5$ sec. At time $t = 0.5$ sec to $t = 1$sec, current decreases to 2A and so power drop occurs.
Figure 9: Current obtained with PI controller

Figure 10: Output voltage and current using PI controller

Figure 11: Output Power using PI controller
4.2 PID Controller

The irradiation estimates utilized in the simulations for example 800 W/m² and 1000 W/m² and its shown in Fig. 12. Fig. 12 shows the irradiance, Input dc voltage and input power of the PV panel. we get a PV voltage \( V_{dc \text{ mean}} \) of 2 kV and the power removed \( P_{dc \text{ mean}} \) from the exhibit is 150 kW When the consistent state is stretched (around \( t = 0.15 \text{ sec.} \)). Fig. 13 shows the voltage and current waveform of PID controller and this PID controller output power is shown in Fig. 14.

![Figure 12: Irradiance, input dc voltage, input power of PV panel](image)

![Figure 13: Current and voltage of converter with PID](image)
4.3 Proposed FoPID Based GWO Technique

Simulink waveform of input power, irradiance, input dc voltage to PV panel based on FOPID controller is shown in Fig. 15. Fig. 16 gives the output voltage of FOPID controller. The output power of the grid connected inverter based on the FOPID controller is 1598 kW and this is shown in Fig. 17. As the active and reactive power output is shown in Fig. 18.

4.4 FOPID Based Fuzzy Logic Controller

Tracking of the highest power point and levels of irradiation below 1000W/m² and 500W/m². In Fig. 19, the current, voltage and power output of the PV system is given along with the after-effect simulation of the PV system with enhanced MPPT-based fuzzy logic control.
Figure 16: Output voltage with FoPID

Figure 17: AC output power of converter with FOPID controller

Figure 18: Active and reactive power output
Fig. 20 shows the input given to fuzzy FOPID controller and the simulink waveform of output voltage, current with Fuzzy FOPID controller is in Fig. 21. Fig. 22 shows Fuzzy based FOPID controller output power of the converter. The output power of the grid connected inverter based on the Fuzzy FOPID controller is 187 kW. The respective solution curve of active and reactive power output from PV system is described in Fig. 23.
4.5 Comparison of the Proposed Work

The Fuzzy-based FOPID control output is evaluated from the suggested work and contrasted with that of PI, PID control, and FOPID control respectively. The comparison using GWO techniques is illustrated in Tab. 2.

Figure 21: Output voltage, current with Fuzzy FOPID controller

Figure 22: AC output power of converter using fuzzy FOPID controller
The efficiency comparison graph is shown in Fig. 24. It is inferred that the proposed Fuzzy FOPID outperforms other algorithms in terms of efficiency.
5 Conclusion

A Fuzzy FoPID energy reshaping control is designed and intended for a grid-connected PV inverter in electric vehicles to optimally extract PV energy under different operating conditions. The performance of current control loop in a three-phase grid-connected PV system has been improved. The performance of current control loop and voltage regulation in a three-phase grid-connected PV system has been dissected. The optimization technique Simulink results show that under different atmospheric conditions, Fuzzy FoPID control can achieve superior control efficiency of 98% with the low control costs as compared to the techniques existing in the literatures. The inverter design in the proposed research can be effectively used in electric vehicles.

6 Future Work

The efficiency of current control loops in a three-phase grid-connected PV system has been enhanced by using a fractional order PID controller with other optimization techniques.

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