THE PHYSICAL PROPERTIES OF THE RED SUPERGIANT WOH G64: THE LARGEST STAR KNOWN?∗

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ABSTRACT

WOH G64 is an unusual red supergiant (RSG) in the Large Magellanic Cloud (LMC), with a number of properties that set it apart from the rest of the LMC RSG population, including a thick circumstellar dust torus, an unusually late spectral type, maser activity, and nebular emission lines. Its reported physical properties are also extreme, including the largest radius for any star known and an effective temperature that is much cooler than other RSGs in the LMC, both of which are at variance with stellar evolutionary theory. We fit moderate-resolution optical spectroscopy of WOH G64 with the MARCS stellar atmosphere models, determining an effective temperature of 3400 ± 25 K. We obtain a similar result from the star’s broadband V – K colors. With this effective temperature, and taking into account the flux contribution from the asymmetric circumstellar dust envelope, we calculate log(L/L⊙) = 5.45 ± 0.05 for WOH G64, quite similar to the luminosity reported by Ohnaka and collaborators based on their radiative transfer modeling of the star’s dust torus. We determine a radius of R/R⊙ = 1540, bringing the size of WOH G64 and its position on the Hertzsprung–Russell diagram into agreement with the largest known Galactic RSGs, although it is still extreme for the LMC. In addition, we use the Ca ii triplet absorption feature to determine a radial velocity of 294 ± 2 km s−1 for the star; this is the same radial velocity as the rotating gas in the LMC’s disk, which confirms its membership in the LMC and precludes it from being an unusual Galactic halo giant. Finally, we describe the star’s unusual nebula emission spectrum; the gas is nitrogen-rich and shock-heated, and displays a radial velocity that is significantly more positive than the star itself by 50 km s−1.

Key words: stars: evolution – stars: late-type – stars: mass loss – supergiants

Online-only material: color figures

1. INTRODUCTION

Red supergiants (RSGs) are an evolved He-burning phase in the life of a moderately massive star (10–25 M⊙). Their location in the Hertzsprung–Russell (H–R) diagram has, in the past, been at odds with the predictions of stellar evolutionary theory, occupying a position that was too cold and too luminous to agree with the position of the evolutionary tracks. Levesque et al. (2005, 2006; hereafter Papers I and II) and Massey et al. (2009) have used the newest generation of the MARCS stellar atmosphere models (Gustafsson et al. 1975, 2003, 2008; Plez et al. 1992; Plez 2003) to fit model spectral energy distributions (SEDs) to moderate-resolution spectroscopy of RSGs in the Milky Way, Magellanic Clouds, and M31. The new physical parameters derived from this fitting shifted the properties of RSGs to higher effective temperatures and lower luminosities, bringing them into generally excellent agreement with the evolutionary tracks.

However, the RSGs include several oddball members that require a more detailed analysis. One classic example is the case of VY CMa, a well-studied dust-enshrouded RSG in the Milky Way. Massey et al. (2006) fit a spectrum of VY CMa with the MARCS models and derived an effective temperature (Teff) that was much warmer than previous estimates (Le Sidaner & Le Bertre 1996) and brought this previously troublesome star into much better agreement with the evolutionary tracks; however, determination of VY CMa’s stellar luminosity remains difficult due to the challenges posed by the large structured dust-reflection nebula that surrounds the star (Monnier et al. 1999; Smith et al. 2001; Smith 2004; Humphreys et al. 2005; Massey et al. 2008) and its uncertain distance (Choi et al. 2008). Another example is the unusual Magellanic Cloud RSGs with variable effective temperatures and dust production as described in Levesque et al. (2007) and Massey et al. (2007), and henceforth referred to as Levesque–Massey variables. These stars show considerable changes in their effective temperatures and V magnitudes and a common set of variations—when they are at their warmest they are also brighter, dustier, and more luminous. They are recognizable in their cooler states by occupying the “forbidden” region on the H–R diagram to the right of the Hayashi track, where stars are no longer expected to be in hydrostatic equilibrium (Hayashi & Hoshi 1961). They are currently believed to be in an unstable (and short-lived) evolutionary phase not previously observed in RSGs.

WOH G64 (α2000 = 04:55:10.49, δ2000 = −68:20:29.8, from Buchanan et al. 2006) is another unusual RSG in the Large Magellanic Cloud (LMC), originally discovered by Westerlund et al. (1981), with a number of properties that set it apart from the rest of the LMC RSG population. It is an IRAS source (IRAS 04553−6825), and is surrounded by an optically thick dust torus (Elias et al. 1986; Roche et al. 1993; Ohnaka et al. 2008). Studies of the optical spectra by Elias et al. (1986) and van Loon et al. (2005) show a spectrum dominated by very strong TiO bands, which has led to assignments of spectral types as late as M7–8, by far the latest spectral type assigned to an LMC RSG (e.g., Paper II), with corresponding extreme
physical properties, which would make WOH G64 the star with the largest known radius, and the RSG with the largest known luminosity and mass (van Loon et al. 2005). It is also a known source of OH, SiO, and H$_2$O masers (Wood et al. 1986; van Loon et al. 1996, 1998, 2001), with two different maser components, suggesting a substantial mass outflow and two different expanding dust shells (Marshall et al. 2004). Finally, Elias et al. (1986) report detections of H$_2$, [O i], and [N ii] emission in the optical spectrum. WOH G64 is neither isolated nor in a well-populated region. The star is not in any of the LMC OB associations (Lucke & Hodge 1970).

We have investigated this unique RSG in more detail, applying a similar analysis used in Papers I and II to examine the physical properties that can be derived from the optical spectrum. We obtain moderate-resolution spectrophotometry of WOH G64 using IMACS on the Baade 6.5 m telescope at Las Campanas Observatory (Section 2), confirm this star’s membership in the LMC (Section 3), and compare the parameters that we determine from our model fitting to those presented in past work and predictions of evolutionary theory (Section 4). Finally, we discuss the intriguing issue of emission-line features in WOH G64 (Section 5) and summarize our findings on this unusual star (Section 6).

2. OBSERVATIONS

A flux-calibrated spectrum of WOH G64 was obtained on UT 2008 December 10 using the IMACS spectrometer on the Baade 6.5 m telescope during an observing run primarily devoted to an unrelated project. A 300 line mm$^{-1}$ grating was used in first order for spectral coverage from 3500 Å to 9500 Å. A 0.9-wide long slit was used, resulting in a spectral resolution of 4.3 Å. The observation consisted of 3 × 600 s exposures, and were obtained under photometric conditions. The seeing, measured in the visible off the guide camera (which is off-axis) and were obtained under photometric conditions. The seeing, away, or the star BI 23, classified as B0 II by Conti et al. 1986, is known luminosity and mass (van Loon et al. 2005). It is also with the largest known radius, and the RSG with the largest

The spectra were first normalized to unity, and then a value of 1 subtracted so that only spectral features add signal to the cross correlation. We used the three individual WOH G64 spectra in order to determine the internal consistency of our velocity measurements; in addition, we cross correlated each of the radial velocity “standards” against each other. These tests revealed that the maximum difference seen in cross correlating any two calibrating stars against themselves was 10 km s$^{-1}$, giving us assurance that the velocity we determine with the combination of the three would be a few km s$^{-1}$. We expect to be able to centroid each line to about 10% of the spectral resolution element or better, and so this is consistent since the 4.3 Å resolution translates to about 150 km s$^{-1}$. We obtained a radial velocity of 294 ± 2 km s$^{-1}$, where the error refers to the formal standard deviation of the mean, and reflects the good agreement in cross correlating the stars used for the velocity determinations against themselves. Given this star’s location in the LMC, we expect a heliocentric velocity of 263 km s$^{-1}$ due to contributions from the LMC’s space motion relative to the Sun and its internal rotation, using a kinematic model fit to LMC carbon stars (Olsen & Massey 2007). Although our measured velocity for WOH

3. MEMBERSHIP IN THE LMC

Before investigating the physical properties of WOH G64, we first wished to confirm that it was indeed an RSG member of the Magellanic Clouds, rather than an unusual foreground giant. Elias et al. (1986) measure a radial velocity of 315 km s$^{-1}$ from several nebular emission lines, but state that the velocity zero point is uncertain by 50 km s$^{-1}$, and cite this as evidence of membership in the LMC. However, this really only demonstrates that the star is not a foreground dwarf; a halo giant will have a similar velocity to the LMC’s systematic velocity, as it is due mainly to the reflex motion of the Sun. This value can also be compared to the ∼270–278 km s$^{-1}$ velocity of the maser emission reported by Marshall et al. (2004), which is more in line with our expectations of the LMC’s rotation (Olsen & Massey 2007). Finally, van Loon et al. (1998) use the Ca ii triplet to measure a heliocentric velocity of ∼300 km s$^{-1}$.

We can use our spectra to determine if the star’s radial velocity is consistent with the kinematics of other RSGs in the LMC. We measured the radial velocity of WOH G64 by cross correlating our spectra against those of three LMC RSGs with accurate velocities measured by Massey & Olsen (2003), [M2002] LMC 022204, 024014, and 024987. For this, we used the fxcor task in the IRAF rv package, restricting the cross-correlation region to 8450–8700 Å, which contains the very strong Ca ii triplet lines at λλ 8498, 8542, 8662 (Figure 1). The spectra were first normalized to unity, and then a value of 1 subtracted so that only spectral features add signal to the cross correlation. We used the three individual WOH G64 spectra in order to determine the internal consistency of our measurements; in addition, we cross correlated each of the radial velocity “standards” against each other. These tests revealed that the maximum difference seen in cross correlating any two calibrating stars against themselves was 10 km s$^{-1}$, giving us assurance that the velocity we determine with the combination of the three would be a few km s$^{-1}$. We expect to be able to centroid each line to about 10% of the spectral resolution element or better, and so this is consistent since the 4.3 Å resolution translates to about 150 km s$^{-1}$. We obtained a radial velocity of 294 ± 2 km s$^{-1}$, where the error refers to the formal standard deviation of the mean, and reflects the good agreement in cross correlating the stars used for the velocity determinations against themselves. Given this star’s location in the LMC, we expect a heliocentric velocity of 263 km s$^{-1}$ due to contributions from the LMC’s space motion relative to the Sun and its internal rotation, using a kinematic model fit to LMC carbon stars (Olsen & Massey 2007). Although our measured velocity for WOH
4. PHYSICAL PROPERTIES

4.1. Previous Work

Elias et al. (1986) obtain a 6200–9200 Å spectrum of WOH G64 from the Cerro Tololo Inter-American Observatory Blanco 4 m and RC Spectrograph. Based on this spectrum, they assign the star a type of \( \sim M7.5 \), and derive an \( M_{\text{bol}} \) of \( -9.7 \) (adopting a distance modulus of 18.6) by integrating over IR ground-based and IRAS data and assuming the \((V-K)\) color to be \( 8 \); we correct this to \( M_{\text{bol}} = -9.6 \) \( (L/L_\odot = 5.4 \times 10^8) \) adopting a distance modulus of 18.5 (van den Bergh 2000). This work is also the first to note the incredible excess IR emission from WOH G64 and postulate that such emission is coming from a substantial circumstellar dust shell.

van Loon et al. (2005) examine a low-resolution long-slit optical spectrum obtained with DFOSC at the 1.5 m Danish telescope at La Silla in 1995 December. They assign a spectral type of M7.5e I, in agreement with Elias et al. (1986), but also find some disagreement between different TiO bands, with the 6200 Å band suggesting an M7–8 I type, while some relative band strengths suggest an earlier type of M5 I. They assign a \( T_{\text{eff}} \) of 3008 K based on a giant-class \( T_{\text{eff}} \) scale published in Fuks et al. (1994) and use of the dust radiative transfer model DUSTY (Ivezić et al. 1999). Finally, they determine \( M_{\text{bol}} = -9.49 \) \( (L/L_\odot = 4.90 \times 10^8) \), adopting a distance to the LMC of 50 kpc.

Most recently, Ohnaka et al. (2008) use 2005 and 2007 N-band observations to compute two-dimensional models of the dusty torus surrounding WOH G64. While Ohnaka et al. (2008) begin by discussing the parameters derived by van Loon et al. (2005) and Elias et al. (1986), the temperatures cited within are not derived from the latter papers; instead, Ohnaka et al. (2008) correlates the spectral type range of M5–7 with \( T_{\text{eff}} \) values of 3200–3400 K. Adopting the 3200 K \( T_{\text{eff}} \) in their radiative transfer modeling, and a distance to the LMC of 50 kpc, they determine an \( M_{\text{bol}} \) of \( -8.9 \) \( (L/L_\odot = 2.8 \times 10^8) \) based on radiative transfer modeling of the dusty torus around the star. They also compute two-dimensional models with \( T_{\text{eff}} = 3400 \) K and find that this affects the resulting parameters very little (Ohnaka et al. 2008). The final luminosity determined from this modeling is a factor of 2 lower than Elias et al. (1986) and van Loon et al.’s (2005) luminosities.

Figure 1. Velocity of WOH G64 compared to the kinematics of the LMC’s H I gas and other LMC RSGs. Left: measured H I velocities (grayscale; Kim et al. 2003) and LMC RSGs (points; Massey & Olsen 2003) have been converted to in-plane circular velocities, as described in Olsen & Massey (2007), and are plotted vs. in-plane radius. The polygons labeled “S,” “E+B,” and “E2” mark the signatures of H I tidal streamers identified by Staveley-Smith et al. (2003) and Olsen & Massey (2007); different colors (green, yellow, and magenta) identify RSGs that fall within these regions. The red polygon outlines the LMC’s flat internal rotation curve. The large blue dot marks WOH G64, which clearly has a velocity typical of RSGs at its in-plane radius. Right: the H I gas contained within the regions drawn at bottom left are plotted with different colors as follows: red for the main rotation curve, magenta for the arm S region, yellow for the combined arm E and B regions, and green for region E2. The blue dot again marks the location of WOH G64, while the remaining points are other LMC RSGs. WOH G64 is coincident with the gas that is rotating in the LMC’s disk.

Figure 2. Optical SED of WOH G64 (black) overplotted with the best-fit MARCS stellar atmosphere model with \( T_{\text{eff}} = 3400 \) K (red); there is good agreement with the depths of the TiO bands at 5167 Å, 5448 Å, 5847 Å, 6158 Å, 6658 Å, and 7054 Å, as well as with the overall continuum. Agreement with the 8433 Å and 8859 Å lines is less satisfactory; however, this is consistent with our past experience that these features are not well matched with the MARCS models (Papers I and II). Nebular emission lines detected in the spectrum are labeled here and include [N ii], [O i], Hα, [N iii], and [S ii]. The gaps in the spectrum at \( \sim 6530 \) Å and 7900 Å are the result of gaps in the IMACS CCD mosaic and do not interfere with our model fitting. The strong feature at 7600 Å is the telluric A band.
4.2. Properties from Spectral Fitting

Based on the strengths of the TiO bands in our WOH G64 optical spectrum, we assign a spectral type of M5 I by comparison with other RSGs we have classified (Papers I and II; Massey et al. 2009). This type confirms WOH G64 as the latest-type RSG in the LMC, although it is considerably earlier than the M7.5 types discussed in Elias et al. (1986) and van Loon et al. (2005).

The observed SED for WOH G64 was compared to MARCS stellar atmosphere models of metallicity $Z/Z_\odot = 0.5$, corresponding to the metallicity of the LMC (Westerlund 1997; Massey et al. 2004). The MARCS model SEDs available ranged from 3000 to 4500 K in 100 K increments, and were interpolated for intermediate temperatures at 25 K increments. The log $g$ values ranged from $-1$ to $+1$ in increments of 0.5 dex. When fitting the models to the data, they were reddened adopting the Cardelli et al. (1989) $R_V = 3.1$ reddening law.

The reddening and $T_{\text{eff}}$ were determined by finding the best by-eye fit between the MARCS models and the WOH G64 SED. The reddening was based on the agreement between the model and observed continuum, while $T_{\text{eff}}$ was based on the strengths of the TiO bands at $\lambda\lambda 6158,6658,7054$ ( Jaschek & Jaschek 1990), with the bluer TiO bands at $\lambda\lambda 5167,5448,5847$ used as secondary confirmations of the fit quality; this ensured that there was minimal degeneracy in determining the best model fit. The $\lambda 8433$ and $\lambda 8859$ TiO bands are present in the spectrum as well; however, we have found in past work that these features are not generally well matched by the MARCS models (see Papers I and II). Considering WOH G64’s strong TiO band strengths and corresponding late spectral type, our precision for this fit was $\pm 25$ K. The extinction value $A_V$ is determined to approximately $0.15$ mag precision.

From fitting the 5000–9000 Å optical spectrum, we find a $T_{\text{eff}}$ of 3400 ± 25 K and $A_V = 6.82 \pm 0.15$ mag, adopting a log $g$ value of $-0.5$ dex. Our best model fit is shown in Figure 2, and alternative model fits demonstrating the precision of these derived properties are shown in Figure 3. In order to confirm that this is the appropriate log $g$ value for WOH G64, we must first determine the star’s radius, which in turn requires calculation of the bolometric luminosity. While RSGs in the LMC are known to be variable by up to a magnitude or more in $V$ (Levesque et al. 2007), their variability at $K$ is much smaller ($\sim 0.2$ mag; Josselin et al. 2000). For this reason, we determine the bolometric luminosity based on WOH G64’s $K$ magnitude. There are a number of $K$-band observations for this star, including $K_s = 6.85$ from Two Micron All Sky Survey (2MASS), $K = 6.85$ from Buchanan et al. (2006), $K = 6.88$ from Elias et al. (1986), and $K = 6.91$ from DENIS (Epchtein et al. 1997). The consistency of these magnitudes confirms that the $K$ magnitude of WOH G64 has stayed quite constant with time. We adopt the 2MASS $K_s$ magnitude for this work, correcting $K_s$ to $K$ by the relation $K = K_s + 0.04$ (Carpenter 2001) and adopting an error of $\pm 0.2$ mag (Josselin et al. 2000). We adopt the $T_{\text{eff}}$-dependent bolometric correction at $K$ for the LMC (Paper II):

$$BC_K = 5.502 - 0.7392 \left( \frac{T_{\text{eff}}}{1000 \text{ K}} \right).$$

By taking these parameters, calculating $A_K = 0.12 \times A_V$ (Schlegel et al. 1998), and adopting a distance modulus of 18.5 (50 kpc) for the LMC (van den Bergh 2000) with an error of $\pm 0.1$ mag, we determine a physical log $g$ of $-0.7 \pm 0.1$ dex, which agrees with our model surface gravity. With these values, and taking $M_{\text{bol,0}} = 4.74$ (Bessell et al. 1998) we also determine an $M_{\text{bol}} = -9.4 \pm 0.3 \left( \text{log}(L/L_\odot) = 5.65 \pm 0.14 \right)$, or $\sim 0.6$ mag more luminous than the value obtained by Ohnaka et al. (2008). We also measure a radius of $R/R_\odot = 1970$, with an uncertainty.
of \( \sim 5\% \). While van Loon et al. (2005) mention some disparity in spectral-type determinations between different TiO bands, we find no such disagreement when assigning our spectral type and \( T_{\text{eff}} \).

### 4.3. Properties from \((V - K)_0\)

As a self-consistency check, we also determine these physical properties based on the \((V - K)_0\) color of WOH G64, as we have done in past papers (Papers I and II; Levesque et al. 2007; Massey et al. 2009). For a \( V \) magnitude, we adopt \( V = 18.63 \) from the MACHO photometric data (Allsman & Axelrod 2001). We deredden the photometry using \((V - K)_0 = V - K - (0.88 \times A_V)\) (Schlegel et al. 1998). From this, we find that \((V - K)_0\) for WOH G64 is 5.74. In Paper II, we determined the theoretical relation between \( T_{\text{eff}}\) and \((V - K)_0\) based on the MARCS models and the assumptions of Bessell et al. (1998) concerning the effective broadband bandpasses, and found

\[
T_{\text{eff}} = 7621.1 - 1737.74(V - K)_0 + 241.762(V - K)_0^2 - 11.8433(V - K)_0^3. \tag{2}
\]

With these we determined a \( T_{\text{eff}} \) of 3372 K. Once again using the bolometric correction at \( K \) and \( A_K \) and propagating our errors for these values, these numbers in turn produce a value of 9.4 \( \pm 0.3 \) \( \log(L/L_\odot) = 5.65 \pm 0.13 \). Based on these parameters, we also calculate a radius of \( R/R_\odot \) of 1990 with an uncertainty of \( \sim 5\% \). This shows excellent agreement between the parameters derived from spectral fitting as compared to the \((V - K)_0\) colors.

The effective temperatures from both spectral fitting and \((V - K)_0\) colors agree with the predictions of the \( T_{\text{eff}} \) scale for the LMC (Paper II); WOH G64 is the only M5 I RSG known in the LMC, and this additional data point agrees nicely with the general trend that the LMC \( T_{\text{eff}} \) scale is \( \sim 50 \) K cooler than the Galactic scale (the single M5 I RSG in the Milky Way, \( \alpha \) Her, has a \( T_{\text{eff}} \) of 3450 K; Paper I).

The parameters determined from past work, our spectral fitting, and our \((V - K)_0\) colors are summarized in Table 1, where we also compare our values to those derived by others.

### 4.4. The Physical Parameters of WOH G64 and the H–R Diagram

In our analysis of WOH G64, we find an unusually high bolometric luminosity, \( M_{\text{bol}} = -9.4 \) (\( \log L/L_\odot = 5.65 \)) compared to the other most luminous RSGs in the Magellanic Clouds (\( M_{\text{bol}} = -8.8 \)). As shown in Table 1, our value is consistent with that of Elias et al. (1986) and van Loon et al. (2005), but about 0.5 mag more luminous than that found by Ohnaka et al. (2008).

As is obvious from the large extinction, WOH G64 is surrounded by a dense circumstellar envelope. If this envelope were spherical, then the flux absorbed along the line of sight would be re-radiated toward us in the NIR, but with an asymptmetrical circumstellar environment (either a torus or a disk), we may receive more (or less) than what is absorbed. If we adopt the geometrical model proposed by Ohnaka et al. (2008), that we view a torus almost head-on, then we are receiving more flux form the combined system (star plus torus) than is being absorbed. Based on Figure 5 in Ohnaka et al. (2008), we estimate the torus contributes approximately 0.5 mag at \( K \). In order to derive the stellar flux, we then need to correct our \( M_{\text{bol}} \) derived from \((V - K)_0\) by this amount, and arrive at an \( M_{\text{bol}} = -8.9 \).

We list our final adopted parameters in Table 1.7

We believe our value for the extinction is to be preferred over that of the Ohnaka et al. (2008) analysis, as they adopt a blackbody flux distribution for the star. The use of a blackbody overestimates the stellar flux in the optical, which leads to an overestimate of the amount of attenuation required to reproduce the observed data. In the end, though, our estimates for the bolometric luminosities are in excellent agreement, as shown in Table 1. Ohnaka et al. (2008) did adopt a somewhat lower \( T_{\text{eff}} \) than what we found (3200 K versus 3400 K), but fortuitously they also applied their analysis with a 3400 K \( T_{\text{eff}} \) and derive essentially the same bolometric luminosity (K. Ohnaka 2009, private communication).

With our determination of \( T_{\text{eff}} = 3400 \) K and \( M_{\text{bol}} = -8.9 \), we derive a stellar radius of 1540 \( R_\odot \). Given the minimum formal errors (\( \Delta T_{\text{eff}} = 25 \) K and \( \Delta M_{\text{bol}} = 0.1 \) mag), the uncertainty of the radius is 5%. This value of 1540 \( R_\odot \) is significantly

\[\text{Note that Humphreys et al. (2007) have argued that Massey et al. (2006) have badly underestimated the actual luminosity of VY CMa, citing as the "fundamental astrophysical basis" for their higher luminosity the integration of the SED, most of which is re-radiated thermal emission from the dust around the star. We note that the Massey et al. (2006) analysis could have been in error if there were substantial gray absorption, i.e., if the circumstellar dust did not follow a Cardelli et al. (1989) \( R_V = 3.1 \) reddening law, which is certainly a possibility. However, it is also true that the argument by Humphreys et al. (2007) rests on the unproven (and unstated) assumption of spherical symmetry for the dust emission.}\]
larger than the largest Magellanic Cloud stars (1240–1310\(R_\odot\), as expected from its cooler temperature and higher bolometric luminosity. But, while the star may be a behemoth by Magellanic Cloud standards, it is about the same size as the largest RSGs we found in Milky Way (Paper I), where KW Sgr, Case 75, KY Cyg, and \(\mu\) Cep all have essentially the same large radii as WOH G64.

In Figure 4, we show the position of the star in the H–R diagram, compared to the location of the Geneva evolutionary tracks. We have included too the locations of the star from van Loon et al. (2005) (filled pentagon), Ohnaka et al. (2008) (filled square), and the parameters adopted in this paper (open star). The position is compared to the locations of the LMC RSG population presented in Paper II, as well as the evolutionary tracks of the Geneva group. Older, nonrotating evolutionary tracks that include the effects of overshooting are shown as solid lines and come from Schaefer et al. (1993); newer rotating evolutionary tracks, when available, are shown as dotted lines and come from Meynet & Maeder (2005). Lines of constant radius are shown by diagonal lines in the upper right. It can be seen that our final parameters are in much better agreement with the position of the other LMC RSGs, and assign WOH G64 a notable smaller radius, although WOH G64 remains the coolest, largest, and most luminous RSG in the LMC.

(A color version of this figure is available in the online journal.)

5. EMISSION LINES IN THE WOH G64 SPECTRUM

Elias et al. (1986) report detection of [O i] \(\lambda\lambda6300, H\alpha, [N\, ii]\), \(\lambda6548, [N\, ii]\), \(\lambda6584, [S\, ii]\), \(\lambda6731\) emission. Using the [O i], H\(\alpha\), and [N ii] lines they measure a radial velocity of 315 km s\(^{-1}\), which implies a redshift compared to the 270–278 km s\(^{-1}\) value found in the maser analysis by Marshall et al. (2004) and our 294 km s\(^{-1}\) measurement from the Ca ii lines (Section 3), given that the Elias et al. (1986) value may have a zero-point error as large as 50 km s\(^{-1}\). Given that the Elias et al. (1986) values have as much as 50 km s\(^{-1}\) zero-point error, the significance of this redshift was not large, but we confirm the redshift below, using more accurate measurements.

In the red part of our spectrum, we detect [O i] \(\lambda\lambda6300, H\alpha, [N\, ii]\) \(\lambda\lambda6548, [N\, ii]\), \(\lambda6584, [S\, ii]\), \(\lambda6731\) emission (Figure 5(a)). The [S ii] \(\lambda6717\) doublet line is not measurable, as its wavelength is coincident with one of the numerous absorption features in our spectrum. In addition, we detect H\(\beta\), [N i] \(\lambda\lambda5198,5200\), and [O iii] \(\lambda5007\) emission in the bluer region of the spectrum (Figure 5(b)). We also note that some of the TiO band heads are in weak emission. This is also seen in at least one other RSG with an extreme circumstellar environment, e.g., VY CMa (Hyland et al. 1969; Wallerstein & Gonzalez 2001). The lines are clearly spatially coincident with the stellar spectrum, and there is no evidence of extended (nebular) emission in our spectra. We would readily detect an extension of 0.3 pixels, corresponding to 0\.'33, or 0.08 pc at the distance of the LMC. We have measured the radial velocities of the emission lines by fitting Gaussians to them, and find an average (heliocentric) value of \(344\pm9\) km s\(^{-1}\), where the error refers to the standard deviation of the mean; radial velocities for each of these features are given in Table 2. This value is significantly

![Figure 4](image-url)Position of WOH G64 on the H–R diagram, based on the parameters derived in van Loon et al. (2005) (filled pentagon), Ohnaka et al. (2008) (filled square), and the parameters adopted in this paper (open star). The position is compared to the locations of the LMC RSG population presented in Paper II, as well as the evolutionary tracks of the Geneva group. Older, nonrotating evolutionary tracks that include the effects of overshooting are shown as solid lines and come from Schaefer et al. (1993); newer rotating evolutionary tracks, when available, are shown as dotted lines and come from Meynet & Maeder (2005). Lines of constant radius are shown by diagonal lines in the upper right. It can be seen that our final parameters are in much better agreement with the position of the other LMC RSGs, and assign WOH G64 a notable smaller radius, although WOH G64 remains the coolest, largest, and most luminous RSG in the LMC.

![Figure 5](image-url)Nebular emission line detections in the blue (upper) and red (lower) optical spectrum of WOH G64.
larger than 294 ± 2 km s⁻¹ we measure for the star itself (Section 3). It is possible that the redshift of these emission lines can be explained in part by scattering of the spectrum by an extended, expanding dust shell, a phenomenon that has previously been observed and described in RSGs (Romanik & Leung 1981, and references therein).

We measure the integrated fluxes of these emission lines, and correct these values for extinction based on the Hα/Hβ emission line ratio, assuming the Balmer decrement for case B recombination (Hα/Hβ = 2.87, following Osterbrock 1989) and the Cardelli et al. (1989) reddening law. We calculate an AV = 1.90, very different than the value determined for the star from our spectral fitting; however, it is not surprising that the gas we observe has a net extinction that is lower than the star, and this is in fact consistent with it forming in the outer part of the dust shell. The observed and dereddened integrated fluxes are included in Table 2.

With these dereddened fluxes, we are able to calculate several common emission line diagnostic ratios, notable log([N II] λ6584/Hα) = 0.05, log([O I] λ6300/Hα) = −0.42, and log([O I] λ5007/Hβ) = −0.58, and a lower limit of log([S II]/Hα) = −0.45 (see Baldwin et al. 1981 for a detailed discussion of these diagnostics). The value of the [O I]/Hα ratio is much higher than the minimum value at which [O I] is considered “present,” defined in Baldwin et al. (1981) as log([O I] λ6300/Hα) = −1.3. This high relative strength of the [O I] line implies that the dominant source of ionization is likely shock heating. This is also implied by the relatively high lower limit of the log([S II]/Hα) = −0.45 ratio in our spectrum (see, for example, Allen et al. 1999, 2008), and we thank the anonymous referee for pointing this out. However, this is not the only explanation, as called to our attention in thoughtful comments by N. Smith (2009, private communication) and P. Bennett (2009, private communication). Bennett argues in particular that such nebular emission is typical of VV Cep-like systems, i.e., formed by ionization by a hot companion, but see discussion below.

We also find that nitrogen is highly enhanced in the nebula; if we use the standard galaxy diagnostics of Pettini & Pagel (2004), which rely upon a constant N/O ratio, we would derive a 12 + log(O/H) = 8.9, considerably in excess of the 12 + log(O/ H) = 8.4 that is typical of H II regions in the LMC (Russell & Dopita 1990). But, far more likely is the possibility that N is simply enhanced in this gas. Without other line diagnostics (such as [O II] λ3727, [O I] λ4363, or [S II] λ6717), we lack a quantitative knowledge of the oxygen abundance, electron density, and electron temperature. However, such N enrichment is a signature of many shells and rings around massive stars, such as Sher 25 (Brandner et al. 1997; Hendry et al. 2008). Sher 25 is a blue supergiant, but is thought to be in a blue loop phase, with the high N-enriched gas ejected during a prior evolutionary phase (Brandner et al. 1997; see also discussion in Smartt et al. 2002; Hendry et al. 2008). Other such examples are also known (Hunter et al. 2008). We note that [N I] λλ5198, 5200 is strongly present. Like the [O I] λ6300 line, this doublet is also collisionally excited (Osterbrock 1989), and we take its strength as further evidence of shocks and nitrogen enrichment, consistent with the above.

### Table 2

| Line ID  | RV (km s⁻¹) | Observed Flux (erg cm⁻² s⁻¹) x 10⁻¹⁵ | Corrected Flux (erg cm⁻² s⁻¹) x 10⁻¹⁵ |
|----------|-------------|-------------------------------------|-------------------------------------|
| Hβ       | 330         | 0.82                                | 6.5                                 |
| [O II] 5007 | 306         | 0.24                                | 1.7                                 |
| [N II] 5199/5202 | ...          | 2.12                                | 13.9                                |
| [O I] 6300 | 336         | 1.53                                | 6.7                                 |
| [N II] 6548 | 371         | 0.72                                | 3.0                                 |
| Hα       | 355         | 4.31                                | 17.8                                |
| [N II] 6854 | 385         | 4.86                                | 20.0                                |
| [S II] 6731 | 326         | 1.59                                | 6.3                                 |

*Note.* a Blend; no radial velocity calculated.

6. DISCUSSION

We have used the MARCS stellar atmospheres and moderate-resolution spectrophotometry and broadband photometry to investigate the physical properties of the enigmatic supergiant WOH G64. In addition, our study conclusively shows that the star is a supergiant member of the LMC, rather than (say) an unusual giant star in our own galaxy’s halo.

Our analysis finds an effective temperature of 3400 ± 25 K, considerably warmer than previous studies have adopted. With our parameters from spectral fitting, and taking into account the additional flux contribution at K from the asymmetric circumstellar dust envelope as seen in Ohnaka et al. (2008), we determine MB bol = −8.9 for WOH G64. While WOH G64 has previously been cited as having a T eff and MB bol that would make it the largest RSG known, those parameters have also placed it at odds with the position of the evolutionary tracks on the H–R diagram. By contrast, our parameters place WOH G64 closer to the predictions of stellar evolutionary theory and in good agreement with other RSGs in the LMC. We determine a stellar radius of R/R⊙ = 1540 which, while still the largest in the LMC, is now in good agreement with the size of other large RSGs (~1420–1520 R⊙; Paper I), given that such radii have 5% errors or larger.

The question still remains as to whether or not WOH G64 is a Levesque–Massey variable. Its extreme physical properties and position on the H–R diagram are similar to those observed in Levesque–Massey variables. However, there is currently no evidence for spectral variability based on past observations; spectra obtained by Elia et al. (1986), van Loon et al. (2005), and this work all show WOH G64 remaining in a consistent, cool, late-M-type state. The disagreement in type between M5 and M7–8 is almost certainly a result of differing methods rather than changes in the spectrum. However, more frequent observations of WOH G64 could well uncover variations in its V magnitude and T eff; data from the All Sky Automated Survey (ASAS) project (Pojmanski 2002) demonstrate that the star’s I magnitude shows considerable variability, but there is no V- or K-band data available. On the other hand, the star’s very high reddening, well-defined dusty torus, and considerable maser activity would be unique among the Levesque–Massey variables; these properties suggest WOH G64’s similarity to the Milky Way’s VY CMa, as well as other dust-enshrouded RSGs with maser activity such as NML Cyg, VX Sgr, and S Per (Schuster et al. 2006).

Finally, we detect a number of emission lines in the WOH G64 optical spectrum, including Hα and Hβ, [O I], [N I], [S II], [N II], and [O I]. The radial velocity of these features, 344 ± 9 km s⁻¹, is considerably greater than the star’s radial velocity, 294 ± 2 km s⁻¹, which may be due to scattering by the expanding dust region. We also note the presence of some TiO band heads in emission. This has been previously seen in the spectrum of VY CMa, which is due to the extreme circumstellar environment. Inspection of our data shows that the emission is not spatially...
extended, and the strength of the [O I] feature suggests that the dominant source of ionization for these features is shock heating.

We cannot reject the possibility that WOH G64 is a binary system, with the nebular component contributed by a hot companion, but we do not favor this interpretation. First is the issue of the nebular radial velocities. We find a significant (50 km s$^{-1}$) velocity difference between the nebular emission and the stellar component, and, at first blush, this might be taken as an indication of binarity; i.e., with the nebula emission (somehow) tracking the motion of the hot component. However, a similar velocity was also noted by Elias et al. (1986). While this could be a coincidence, it certainly does not argue in favor of a binary hypothesis. Besides, in a short-period system we would not expect the ionized gas to be “attached” to the hot star. Rather, we prefer the explanation that the nebular redshift is the result of scattering within the expanding dust shell. We would not expect the ionized gas to be “attached” to the hot star. Rather, we prefer the explanation that the nebular redshift would not be expected from the companion, and—6 for the RSG. Thus, at B, the two stars would be equally bright, as (B - V)$_{B}$ = -0.3 for a late-type O star, while B - V ≈ 2 for an RSG (see Massey 1998a, 1998b; Paper I). However, further investigation into the source of these emission lines will likely require further spectral analyses, as well as observations of WOH G64 in the bluer regions of the spectrum.

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