A Research on Different Filtering Techniques and Neural Networks Methods for Denoising Speech Signals

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Abstract: This paper intends to provide the best suited noise removal technique for de-noising and retrieving clean speech from a noisy speech signal. The aim is to use different denoising techniques and compare their performance and arrive at a conclusion regarding which one of them is best suited for enhancing voice signals. The analysis is done by evaluating the performance of different denoising techniques for different types of speech samples. This evaluation is done by adding random noise to speech signal then applying denoising techniques to get denoised speech signal. A parallelism is drawn between original signal and denoised signal through evaluation parameters such as SNR and PSNR. The denoising methods are broadly classified as ‘The Filtering Methods’ and ‘The Neural Network Methods’. Under filtering methods four different denoising methods have been used. The four different denoising methods are – Adaptive Filter based on LMS Algorithm, Weiner Filter, Chebyshev Filter and Kalman Filter. Under neural network methods we use three different denoising methods ‘ADALINE’ and two deep learning methods with ‘Fully Connected’ and ‘Fully Convolutional’ neural networks. The performance estimation is done based on variation of evaluation parameters (SNR and PSNR values) for different denoising techniques.

Keywords — Speech denoising techniques, SNR and PSNR evaluation, Filtering techniques, Neural Networks techniques

INTRODUCTION

The fundamental senses are hearing, sight, smell, taste and touch. These senses perceive the information from the environment and human brain processes this information to create a precise response. The complex communication between humans and their environment is aided by these senses. Sound acts as an information provider to these senses. The information has to be noise free for us to better understand the external environment. Noise can be described as any unwanted information which hinders the ability of the human body to process the valuable sensory information. Hence a noise free sound becomes essential for proper interaction of humans with their external world. The primary focus is on speech signals which are information providers in various communication systems. During the transfer of signals, distortion by some unwanted signals causes loss of useful data and information stored in the signals. There are many real time noise signals such as the noise of a train, traffic jam, washing machine and turbines etc. which have to be reduced to retrieve the wanted information.

Speech signals are non-stationary, one dimensional signals produced by employing the speaker’s lips, tongue, cheeks and nose. The frequency of speech signals ranges from 85Hz to 255 Hz. Typical male voices range lie in the lower frequency range between 85-180 Hertz whereas the female voices fall in the higher range of 165-255Hz. Babies have even higher ranges of frequency reaching up to 1000Hz in a few cases. The sound is created by changing the air pressure with time. [2][3] This fluctuation in air pressure is captured in terms of voltages and currents to form electrical signals by microphones. When the voice signal is thus captured and communicated, it is often riddled with noise.

In the paper, the noise is added to a clean audio signal and then it is passed through the filter to obtain the denoised audio. The parameters being used to gauge the performance of the filters are PSNR and SNR. The motive is to obtain the best SNR and PSNR values for different types of sample speech signals and to provide the best suitable noise reduction method for a particular sample signal. There are variety of human spoken languages, each with different sound characteristics such as pitch, separation between vocal folds, tones etc. hence the speech signals contains samples of different languages in both male and female voice. The analysis of each noise cancellation methods, to put forward both its positive and negative aspects along with its compatibility with sample signals is the main focus of this paper. The noise cancellation techniques have various real time applications, but often the implementation of these methods is challenging. Efforts have been made in this aspect by introducing artificial neural networks to provide noise free speech signals and working with noises we hear on a daily basis.

$$\text{SNR}= 20 \times \log_{10} \frac{\text{PNS SIGNAL}}{\text{THIS NOISE}}$$

$$\text{PSNR}= 20 \times \log_{10} \frac{\text{MAX}}{\text{MSDE}}$$

There are many methods available for noise cancellation in speech signal. This paper has a motive to provide a brief overview and working of few signal processing and neural network de-noising techniques, to bring out the characteristics and functionality of these techniques. This is done by testing the techniques with hundreds of sample signals and to analyse about the suitability of these methods for different types of samples.

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II. THE FILTERING METHOD

There are different filters used for de-noising speech signals. The filters that have been used are - Adaptive Filter using LMS (least mean square) algorithm, Weiner Filter, Chebyshev Filter and Kalman Filter.

A. Adaptive Filter using LMS Algorithm

Adaptive filter is like any other linear filter except that its transfer function is variable. It can be changed by adjusting some parameters. An error signal is generated by comparing the input signal and training signal and this is used to adjust the parameters. Thus, adaptive filters regulate themselves in accordance with the incoming signal. Adaptive filters have an algorithm to optimize the parameter’s values. The LMS (Least mean square) algorithm employs the stochastic gradient descent technique. This means that the filter coefficients are only affected by the current value of error. As its name suggests the filter coefficients are directly related to the least mean square of the difference between the signal we desire and the original signal. The primary principle behind this approach is to keep updating the filter weights until they reach their optimum value. Initially, very small values are assigned to the weights and they are updated according to the MSE (Mean Square Error) gradient. The filter is adjusted to minimize the output power and the output noise power is also minimized. Hence by minimizing the total output power the filter maximizes the output signal-to-noise ratio.

While selecting the step size in the LMS algorithm one needs to be careful because if the step size is large the dependence of the weights on the gradient increases, so any minor change in the gradient would lead to oscillation of the weights. However, if the step size is too small the weights will take a very long duration of time to reach the ideal weight values.

### Table 1 Variation of MSE with Variation in Step Size

| STEP SIZE | MEAN SQUARE ERROR |
|-----------|-------------------|
| 0.01      | 5.43×10^-5       |
| 0.06      | 1.88×10^-4       |
| 0.1       | 3.83×10^-3       |
| 0.5       | 0.0029            |
| 1         | 0.0046            |
| 5         | 0.0062            |

The results of Adaptive Filter using LMS algorithm with graphs of the original, noisy, reference input denoised signals and the MSE plot have been illustrated below.

![Fig. 1 Adaptive filter using LMS algorithm](image1.png)

![Fig. 2 Original and Noisy Speeches](image2.png)

![Fig. 3 Mean Square Error](image3.png)
The adaptive filter using LMS algorithm cancels the noise from a noisy speech signal. The major advantage of this method include its ability to adapt to the noise, its tendency to provide output signals with low noise and to be able to do this without distorting the signal. Being an adaptive filter it can eliminate the unpredicted noise even when it has non-stationary properties.

**B. Weiner Filter**

Among the numerous techniques developed for noise cancellation one of the most fundamental is the Weiner filter. This filter reduces noise by drawing a comparison between the received signal and the estimate of the noiseless signal that we desire. However, in this filter the input is assumed to be stationary. For its implementation it is eminent that the user is aware of spectral properties (power functions etc.) of both the noise and the original audio.[12] The process works based on minimizing the mean square error between the new signal and the original signal. It is widely known that though the Weiner filter reduces the noise it comes at the cost of speech distortion. Therefore, it is only advised to use this filter when the noise cancellation-speech distortion trade-off is acceptable.

In this method Weiner filter is using the TSNR (Two Step Noise Reduction) Method. The signal observed is the combination of the clean audio and the noise. This speech is broken down into tiny frames. These frames are then overlapped with the successive frames. Each of them is smoothed using a Hamming window. Then using Fast Fourier Transform, the signal is converted from the time domain to the frequency domain. Phase and Magnitude are extracted from the FFT so obtained. The required modification to their value is calculated using the TSNR method. Once new phase and magnitude are obtained, their IFFT (Inverse Fast Fourier Transform) is calculated and the frames are overlapped and added to produce the denoised speech signal. [13]
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The Weiner filter is the most fundamental technique used for noise cancellation in speech signals. This method causes speech degradation which reduces SNR and PSNR values. Hence, this method cannot be applicable for real time applications. However, there are some measures which performance of the filter by relating the amount of speech distortion with noise reduction factors. The error is also relatively high as compared to other signals. Hence, it is not recommended to use this filter for noise cancellation in speech signals.

C. Chebyshev Filter

Chebyshev filters are very attractive as they are able to allow a particular band of frequency pass while blocking all others. Another advantage with these filters is that the time taken to process the signal is very less. This is because the Chebyshev filter’s transition between its passband and stopband is extremely quick. However, these filters introduce ripples. The original audio file, which is in the .wav format is inputted into MATLAB. A random noise signal is added to the original audio. The input signal’s frequency is set as the sampling frequency. The other parameters such as the Nyquist Frequency Fn, the passband frequency Wp, the stopband frequency Ws, the passband ripple Rp and the stopband ripple Rs are duly assigned. (In this particular paper their values are as Fn = (Sampling Frequency)/2, Wp = 1000/Fn; Ws = 1010/Fn; Rp = 1; Rs = 15). The filter is then designed using the inbuilt command in MATLAB. To double the order of the filter, zero phase digital filtering is used. Finally, the noisy audio is passed through the filter and a de-noised signal is obtained.

The results of Chebyshev Filter with graphs of the original, noisy, denoised signals and the MSE plot have been illustrated below.
A digital Chebyshev type 2 low pass filter for de-noising the speech signal is designed. In this, it is difficult to de-noise the speech signal without affecting its quality. Hence the output signal from the filter has large mean square error. Because of high means square error value the SNR and PSNR values are low but the computational time is very small as compared to other filters.

D. Kalman Filter

The Kalman filter is a mathematical method of estimating the state of a phenomenon by minimizing the mean square error of the process. It can predict the past, current and succeeding values without a precise knowledge of the system model. The main idea of the Kalman filter is to predict the future original values from the present and previous values in a reiterative way. This method is usually used when there is uncertainty in information. When the required data cannot be retrieved directly we use Kalman filter. In some situations there is unavailability of the required data hence the available data which is close to the actual data is used as input in Kalman filter. It estimates how a signal is going to behave in future. It is ideal filter for non-stationary signals. [5] Here, Kalman filter has been used to filter out random noise from a speech signal.

The process employed in this algorithm, which is recurrent, occurs in two steps. The first step is ‘the prediction’ wherein the filter generates estimates of the present state variables, including the uncertainties they are associated with. The second step is called ‘the estimation’. Based on the next measurement’s outcome the estimates are updated with the weighted average. Higher weights are assigned to estimates with greater certainty. [6]

The results of Kalman Filter with graphs of the original, noisy, denoised signals and the MSE plot have been illustrated below.
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III. THE NEURAL NETWORK METHOD & RESULTS

In artificial neural network method a basic algorithm – ADALINE (Adaptive Linear Neuron) is used for noise cancellation. The second method includes de-noising the speech signals using deep learning. There are two types of deep learning networks used for de-noising speech signals. The first deep learning method is by using fully connected layers neural networks and the second method includes using convolution layers neural networks for speech signals de-noising.

Deep learning, otherwise called hierarchical learning, uses logic just like human brain to process the data. Deep learning model examines the data using ANN. ANN functions as an algorithm having layered structure to extract ‘information’ from the data. This information is specific features of data. This information is extracted piece by piece by each layer. Each layer brings out different features from a data set. [16] Hence DL is a hierarchical model having multiple levels of abstraction. DL networks are prior trained by past experiences. Neural networks are substructure in deep learning to process the data and extract information. Neural networks use neurons as network of connection to transfer the data as input and output values. They take many data sets as training example and build a system which can identify a feature from the training sets. They do not possess any past information about the data but develops a structure for feature identification from the data. [17]

A. ADALINE

Adaptive Linear Neuron, otherwise called ADALINE is a single layered neural network. Its structure consists of a feedback which enables one to compare the current output with the value that is desired. Once the values are compared (based on the training algorithm), updating of bias and weights takes place. It calculates the sum of products using weight vectors and input and gives a single output value. It uses the delta rule to modify the rates iteratively and hence this neural network is able to respond to any change in the environment in which it operates. An adaptive ADALINE is designed which is best suited for non-stationary signals. The aim is to modify the weights and biases in a way that it minimizes the sum of square errors between the network output and the targets. It is based on LMS algorithm. A function called ‘adapt’ is used in MATLAB for the same.

The performance of ADALINE neural network is largely dependent on the selection of right learning rate value. The learning rate updates the weights of the network which minimizes the error. The training speed of the neural network is also influenced by the learning rate. The learning rate value should neither be too small nor too large. The paper aims to determine the values of learning rate for which the network de-noises speech signal satisfactorily. [15] The performance of adaptive ADALINE with variation in learning rate is illustrated below. The results of ADALINE is also illustrated below.

Table.2 Variation of MSE and Execution time with variation in learning rate

| LEARNING RATE | MEAN SQUARE ERROR | EXECUTION TIME |
|---------------|-------------------|---------------|
| 0.01          | 0.0022            | 691.315s      |
| 0.05          | 0.0011            | 535.668       |
| 0.08          | 8.68x10^-4        | 468.442       |
| 0.09          | 8.25x10^-4        | 530.239       |
| 0.1           | 7.55x10^-4        | 432.388       |
| 0.2           | 4.58x10^-4        | 450.018       |
| 0.3           | 6.38x10^-4        | 405.501       |
| 0.4           | 0.5279            | 511.479       |

Fig.19 Clean Audio

Fig.20 Audio with added Noise

Fig.21 Denoised signal
The Adaptive ADALINE neural network is designed in MATLAB software. ADALINE is the most basic neural network which can be incorporated for speech de-noising. Being an adaptive linear algorithm it abates the noise from the signal instead of filtering the noise from the noisy signal. The network works well and gives high PSNR and SNR values. The speech distortion is minimal and there is almost insignificant difference between filtered output and original signal. The only drawback of this method is that it is time consuming. The success of this method is highly influenced by the learning rate of the network. From the data it is clear that the learning rate should be in the range of 0.08-0.3, as these learning rates provide low mean square error.

B. Deep Learning Fully Connected and Fully Convolutional Neural Networks.

Fully Connected Network:
The architecture of fully connected neural network contains neurons which are linked with every other neuron in the preceding layer. The connection is developed via weights.

Fully Convolutional Network:
In the architecture of convolutional neural network the neuron has connections only with few neurons from the preceding layer. The weight used in every neuron is the same. It can be said that the neurons are locally connected sharing the layers of weight. [18][19].The CNN has three major layers: the input layer, the output layer and the hidden layer. The hidden layers comprises of the Convolutional layer, Activation layer, Pooling layer, Fully Connected layer and Normalised layer. The Convolution Layer merges the data by mathematical operation. In Activation Layer the result from the Convolution layer is passed through the ReLU activation layer. In Pooling Layer the dimensionality of parameters is reduced. The training time is shortened in pooling layer. The Fully Connected Layer converts the three dimension output from pooling layer to a one dimension output and the Normalised Layer normalizes the output.

The audio is transformed into the frequency domain by employing STFT (Short Time Fourier Transform). The window chosen is a hamming with the length being 256 samples and the overlap being 75%. The spectral vector’s size is reduced to 129. Eight successive noisy STFT vectors form the input of the predictor and the estimate each output is calculated using the present noisy vector and the seven previous ones. Here, the predictor is the original signal combined with noise and the target is assumed to be the original audio. To reduce the amount of computation involved, both the original and noisy audios are down sampled to 8 Kilo Hertz. The predictor is magnitude spectrum of noisy signal, the Target is the magnitude spectrum of clean signal, and the output is the magnitude spectrum of denoised signal.

A regression network is used to reduce the MSE (Mean Square Error) between output and target as much as possible. By making use of the magnitude spectrum of the output and the noisy signal’s phase, the denoised speech is obtained in the time domain. The results of the deep learning methods using Fully connected and Fully Convolutional Neural Networks are illustrated below.
The main motive behind working with deep learning techniques is to be able to filter out real time noises such as noise of the washing machine, train etc. from the speech signal. This method has given mediocrity results, the SNR and PSNR values are not very high but the de-noised signal has similarity with the original clean speech signal. This method has given mediocre results, the SNR and PSNR values are not very high but the de-noised signal has similarity with the original clean speech signal. The execution time is very large in deep learning; however the results are not satisfactory. Hence, deep learning de-noising methods cannot be used for speech applications.

### IV. CONCLUSION

After running 100 voice samples through each of the filters, the average PSNR and SNR values for each were calculated. They are as follows:

| PSNR   | SNR   |
|--------|-------|
| 25.6543| 4.9769|
| 32.3139| 5.8657|
| 28.5387| 4.6798|
| 26.4285| 5.1652|
| 23.6139| 4.3811|

Table 3: PSNR and SNR values for fully connected deep learning method

The detailed analysis of each filtering method is done and a comparison has been drawn based on performance of each de-noising technique. The paper arrived at a conclusion that the Adaptive filter using LMS algorithm is the best suited de-noising technique for most of the speech signals. Among the neural network methods, ADALINE gives best results. ADALINE uses adaptive LMS algorithm to minimize error between network output and the targets. However, the main difference in performance of filtering and neural network de-noising methods is that the neural networks have longer execution time compared to the filtering methods. The deep learning de-noising technique is the most complex method of all. The execution time is very large in deep learning; however the results are not satisfactory. Hence, deep learning de-noising methods cannot be used for speech applications.

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