LETTER TO THE EDITOR

Close encounters with the Death Star: Interactions between collapsed bodies and the Solar System

Václav Pavlík¹,² and Steven N. Shore³,⁴

¹ Indiana University, Department of Astronomy, Swain Hall West, 727 E 3rd Street, Bloomington, IN 47405, USA
e-mail: vpavlik@iu.edu
² Astronomical Institute of the Czech Academy of Sciences, Boční II 1401, 141 31 Prague 4, Czech Republic
³ Dipartimento di Fisica, Università di Pisa, Largo B. Pontecorvo 3, Pisa 6127, Italy
⁴ INFN, Sezione di Pisa, Largo B. Pontecorvo 3, Pisa 6127, Italy

Received 30 January 2021 / Accepted 22 March 2021

ABSTRACT

Aims. We aim to investigate the consequences of a fast massive stellar remnant – a black hole (BH) or a neutron star (NS) – encountering a planetary system.

Methods. We modelled a close encounter between the actual Solar System (SS) and a 2 M☉ NS and a 10 M☉ BH, using a few-body symplectic integrator. We used a range of impact parameters, orbital phases at the start of the simulation derived from the current SS orbital parameters, encounter velocities, and incidence angles relative to the plane of the SS.

Results. We give the distribution of possible outcomes, such as when the SS remains bound, when it suffers a partial or complete disruption, and in which cases the intruder is able to capture one or more planets, yielding planetary systems around a BH or a NS. We also show examples of the long-term stability of the captured planetary systems.

Key words. methods: numerical – planets and satellites: dynamical evolution and stability – stars: individual: Betelgeuse – stars: black holes – pulsars: general

1. Introduction

Observations have shown that the compact objects produced by supernova (SN) explosions – neutron stars (NSs) or black holes (BHs) – can receive natal recoil impulses due to intrinsic asymmetries of their birth event. The best-fit observational velocity distribution of these kicks for NSs is a Maxwellian (Hansen & Phinney 1997; Jonker & Nelemans 2004) with a mean velocity about 300 km s⁻¹ and a dispersion of about σₓ = 190 km s⁻¹. A BH could receive a kick of the same magnitude as a NS (Jonker & Nelemans 2004; Repetto et al. 2017); although, more recent investigations argue that lower velocities, for example ~50 km s⁻¹, may be needed to explain the retention fraction of BHs in Galactic globular clusters (Peuten et al. 2016; Baumgardt & Sollima 2017; Pavlík et al. 2018), and that they are likely reduced by the fallback of mass onto the BH remnant (e.g. Belczynski et al. 2008; Fryer et al. 2012).

In this work, we focus on the dynamical consequences of a passage of a collapsed fast moving massive body close to a planetary system using the current Solar System (SS) for realistic initial conditions. Such an event, which could more likely play out in the environment of a star cluster or an association, has hitherto not been fully examined.

Published studies of the stability of planetary systems undergoing stellar encounters have analysed isolated in-plane events involving low-mass single field stars or binaries (e.g. Li & Adams 2015; Malmberg et al. 2011) or have been sited in clusters with the impactor velocity taken from the virialised velocity dispersion using Monte Carlo or N-body procedures on fictitious planetary systems (e.g. Cai et al. 2017; Wang et al. 2020). Our study differs in assuming (1) the real SS with all eight planets, (2) arbitrary off-plane interactions, (3) a massive intruder of high mass ratio, and (4) a broad range of impact parameters and encounter velocities. The only study similar in spirit to ours, by Laughlin & Adams (2000), imposed an approximation of the SS and included high-velocity encounters with a low-mass binary system as the impactor.

2. Simulation methods

The set of nearly 2000 numerical simulations we performed in this study examined two encounter scenarios – BH and NS. We varied the impact parameter, b_I (defined in the plane of the SS), the encounter velocity, v_I, the intruder mass, m_I, and incidence angle, θ_I (relative to the invariable plane of the SS); the subscript ‘I’ specifies the nature of the impactor: BH and NS. No relativistic effects were considered, so the designations BH and NS are formal and indicate a point mass.

Our simulations were performed using REBOUND (Rein & Liu 2012), a symplectic N-body code, with a 15th order Gauss–Radau integrator IAS15 (Rein & Spiegel 2015), which was implemented for Python, and they were analysed using Python with NumPy (Harris et al. 2020) and Matplotlib (Hunter 2007). The system was initiated in isolation, ignoring the Galactic gravitational potential and the very low stellar density in the Solar neighbourhood. The duration of the interaction is much lower than the Galactic orbital timescale of the whole system. The initial
conditions for specific encounter scenarios are described below in further detail.

2.1. Initial conditions

We adopted the same range of impact parameters in both scenarios, \( 10^{-1} \leq b_1 / \text{pc} \leq 10^{-6} \) (the smallest, 0.3 au, is approximately the current orbit of Mercury). The SN kicks may not be the only reason for these encounters, they may also arise in a dynamical system (e.g. a star cluster or an association, as analysed by numerical models Spurzem et al. 2009; Hao et al. 2013; Zheng et al. 2015; Shara et al. 2016; Cai et al. 2017), so we chose velocities 10, 50, and 100 km s\(^{-1}\) we included 360 km s\(^{-1}\) for the NS to account for possibly large velocity kicks or hyper-velocity stars. We also varied the impactor incidence angle, \( \theta \), between 0° and 180° in 30° increments. In each setup, we launched the impactor from 0.5 pc towards the Sun and ended the simulation when the separation of these two bodies was again greater than 0.5 pc, since there was no effect at a larger distance\(^1\).

The initial positions of the planets and the Sun were taken from NASA JPL HORIZONS system for Jan 1, 2000 and then varied in each realisation by letting the SS evolve for a certain amount of time before the start of the simulation. We adopted nine pre-evolved states, evenly distributed from 0 to 165 years (approximately the orbital period of Neptune), producing an ensemble of possible encounters of the remnant with large planets. Such a coarse time step can initially create degenerate positions of the terrestrial planets but can be justified due to the following reasons:

1. We let the massive body travel at different velocities from the same distance, so the positions of planets during the closest approach are different despite starting from the same pre-evolved state.

2. We made several simulations without terrestrial planets. Using deterministic symplectic methods allowed us to make one-to-one comparisons to the simulations with all planets and the same initial configuration. The results show that large gas planets are the dominant agents when it comes to the stability of the SS or capture of planets. Low-mass terrestrial planets being retained, captured, or ejected is a secondary outcome that influences the orbital parameters of the final system should they be captured or retained. Hence, the terrestrial planets behave essentially as test masses. We plotted one such comparison in Fig. 1 – the simulations are almost identical except for the capture of Venus and Earth and a slightly different semi-major axis of Saturn.

3. We also performed high-resolution calculations of the BH encounter, with a fixed incidence angle and a time step between realisations of 0.5 year (i.e. 330 simulations in total, see Appendix A).

2.2. Orbital parameters

For analysing the simulation outputs, we distinguished planets that remained bound to the Sun from those captured by the intruder. We counted all the orbiting bodies within a radius of 200 au around the relevant central object that remained bound until the end of the simulation. The orbital parameters are defined as follows. The semi-major axis is given by

\[
a = \left( \frac{2}{|r|} - \frac{|v|^2}{GM} \right)^{-1},
\]

where \( r \) and \( v \) are the radius and velocity vectors, respectively, in the co-moving frame of the central body (the Sun or the impactor), \( G \) is the Newtonian gravitational constant, and \( M \) is the mass of the central body. The orbital inclination is defined by

\[
i = \arccos \left( \frac{h_z}{|h|} \right),
\]

where \( h = r \times v \) in the co-moving frame, and the eccentricity vector is

\[
e = \frac{v \times h}{GM} - \frac{r}{|r|},
\]

where the orbital eccentricity is \( e = |e| \). These values are plotted for each planet (labelled as Mercury \( \text{M} \), Venus \( \text{V} \), Earth \( \text{B} \), Mars \( \text{B} \), Jupiter \( \text{J} \), Saturn \( \text{S} \), Uranus \( \text{U} \), and Neptune \( \text{N} \)) that has been captured or retained in the top six rows of Figs. 2 and 3 and in Figs. A.2, B.3–B.8, and C.3–C.8. We emphasise that these plots show the distribution of orbital parameters, but not the actual number of captured or retained planets, which is plotted, for example, in Figs. B.1, B.2, C.1, and C.2.

3. Results

Encounters with field stars have been simulated previously, but none specifically assumed that the intruder is a massive compact object. We therefore explored its interaction with a planetary system for arbitrary incidence angles which is likely in denser environments, for example, star clusters (Varri et al. 2018) or the Galactic bulge, where thousands of NSs may be present (e.g. Fragione et al. 2018). The encounter velocities originating from SN kicks will be significantly higher than the virialised velocities that have been used in published simulations (e.g. Wang et al. 2020). In fact, they are closer to what would be expected for a high-velocity star in the Solar neighbourhood (Laughlin & Adams 2000). An estimate of the gravitational capture distance, assuming that the intruder can be bound in the centre of mass frame, is given by

\[
r_{\text{grav}} = 2G (m_1 + M_\odot) / v_1^2.
\]

This scales as

\[
r_{\text{grav}} = 2.4 \times 10^{-7} \left( 1 + \frac{m_1}{M_\odot} \right) \left( \frac{v_1}{190 \, \text{km s}^{-1}} \right)^{-2} \text{pc},
\]

where ‘I’ represents the impactor. For reference, the value for the lowest velocities in our simulations is \( r_{\text{grav,BH}} \approx 10^{-3} \) pc and \( r_{\text{grav,NS}} \approx 2 \times 10^{-4} \) pc.

For \( b_{\text{BH,NS}} \leq r_{\text{grav}} \), we found alterations in both the inclination and eccentricity of virtually all retained planets regardless of the incidence angle and encounter velocity (see Appendices B and C). The most efficient captures for both scenarios occurred in the range 60° ≤ \( b_{\text{BH,NS}} \) ≤ 120°, with up to eight planets for \( b_{\text{BH,NS}} \leq 10^{-5} \) pc and the lowest impact velocity (see \( f_{\text{cap}} \) in Figs. 2 and 3). Eccentricities of the captured planetary orbits, \( e_{\text{cap}} \), were very high – around 0.8 for the BH and 0.65 for the NS.

There was a difference between the prograde (\( b_{\text{BH,NS}} = 0° \)) and retrograde (\( b_{\text{BH,NS}} = 180° \)) encounters with the SS in both scenarios. A low-velocity NS showed no directional preferences for planetary capture, but it was most destructive for a retrograde fly-by with \( b_{\text{NS}} \leq 10^{-5} \) pc; in 60% of the cases, the SS did not

\(^1\) For two models, we also examined the longer-term stability of the captured systems, see Sect. 3.
survive and in the remaining 40% the Sun was left with only one terrestrial planet (see \( f_{\text{ret}} \) and \( f_{\text{cap}} \) in Fig. 3). In contrast, a low-velocity BH was generally more disruptive and also more efficient in capturing planets for a prograde encounter (see \( f_{\text{ret}} \) and \( f_{\text{cap}} \) in Fig. 2).

The greatest difference between the NS and BH case was found in the change of the orbital inclinations of the retained planets, \( i_{\text{ret}} \), as the BH is more likely to completely flip the orbits of even massive planets. Based on the positions of the planets during the encounter, both intruders were able to capture planets on prograde, retrograde, or 90° orbits while approaching from \( \theta_{\text{BHNS}} = 0° \) (see \( i_{\text{cap}} \)). It was, however, impossible for the NS to capture a retrograde planet arriving from \( \theta_{\text{NS}} = 180° \).

**Fig. 1.** Sample realisation from the high-resolution study (see Appendix A) with \( v_{\text{BH}} = 10 \text{ km s}^{-1} \) and \( b_{\text{BH}} = 10^{-5} \text{ pc} \); (a) with all planets and (b) without terrestrial planets. Both panels show the trajectories of the planets with coloured lines (Mercury \( \oplus \), Venus \( \oplus \), Earth \( \oplus \), Mars \( \oplus \), Jupiter \( \oplus \), Saturn \( \oplus \), Uranus \( \oplus \), Neptune \( \oplus \)), the Sun (yellow dots), and the BH (black dots). The left panels are plotted in the coordinates fixed to the initial position of the Sun \( (x_0, y_0, z_0) \), in which the impactor arrived from the right-hand side, and the right panels show a detailed view of the final system captured by the BH in its co-moving coordinates \( (x_{\text{BH}}, y_{\text{BH}}, z_{\text{BH}}) \).
Fig. 2. Outcomes of the BH scenario for $v_{\text{BH}} = 10 \text{ km s}^{-1}$. For each impact parameter (coded by colours and symbols) and incidence angle (columns), we plotted the final distribution of semi-major axes, eccentricities, and inclinations of planets that were either retained by the Sun or captured by the BH (top six rows, for each planet from Mercury $\Psi$ to Neptune $\Psi$). Bottom two rows: fraction of retained and captured planets. Each variation in the initial parameters was averaged over nine pre-evolved states of the SS, see Sect. 2. Detailed plots for all $v_{\text{BH}}$ and $\theta_{\text{BH}}$ are in Figs. B.1–B.8.
Fig. 3. Outcomes of the NS scenario for $v_{NS} = 10 \text{ km s}^{-1}$. For each impact parameter (coded by colours and symbols) and incidence angle (columns), we plotted the final distribution of semi-major axes, eccentricities, and inclinations of planets that were either retained by the Sun or captured by the NS (top six rows, for each planet from Mercury \( \Psi \) to Neptune \( \Psi \)). Bottom two rows: fraction of retained and captured planets. Each variation in the initial parameters was averaged over nine pre-evolved states of the SS, see Sect. 2. Detailed plots for all $v_{NS}$ and $\theta_{NS}$ are in Figs. C.1–C.8.
Although the capture process is a many-body interaction, the final orbital angular momentum and semi-major axis of the captured planet scales directly with the mass of the intruder. We also evaluated the three-body interaction of the Sun, Earth, and BH. These did not produce the outcomes we found in the complete simulations, as expected (see, e.g. Binney & Tremaine 2008; Heggie & Hut 2003). This three-body interaction is effectively a two-body encounter because of the large ratios of masses, and the ratio of the impact parameter and the semi-major axis of the Earth’s orbit. Consequently, the outcomes of our simulations require the full interaction of the massive planets.

At the smallest impact parameters and lowest velocities, the semi-major axes of the inner retained planets increased more than those of gas giants (see $a_{ret}$ in Figs. 2 and 3 and Figs. B.3 and C.3). It should be noted, however, that the most frequent outcome was an ejection of the outer planets. Unlike previous studies (Wang et al. 2020), we found no hot Jupiters among the retained systems even for the lowest impact parameters for any incident angle or velocity. We have also compared our NS in-plane encounter with the strong stellar fly-by scenario of Malmberg et al. (2011). They used a schematic system containing only the giant planets, a 1.5 $M_\oplus$ intruder, 100 au for the impact parameter, and 1 km s$^{-1}$ as the velocity at infinity. Our closest model is $b_{NS} = 10^{-4}$ pc and $v_{NS} = 10$ km s$^{-1}$. They found that $\approx 31\%$ of their systems ejected a planet immediately after the fly-by (listed in their Table 1) and we found a similar number, 25%. In contrast, they stated that $\approx 28\%$ of their systems remained stable for up to 100 Myr, while we have no intact systems for any incidence angle. This difference is due to our higher impactor velocity and mass. Malmberg et al. (2011) do not provide the statistics on capture by the intruder, but we see $\geq 45\%$ cases where the NS has captured at least one planet, so the lack of stable systems is partly accounted for by this phenomenon rather than planetary ejection.

We also performed two long-term (>1 Myr) integrations, one for each impactor, to examine the stability of the captured systems. Both had captured Jupiter and three terrestrial planets. The NS was an orthogonal incidence, while the BH was from the high-resolution study described in Appendix A. In both cases, all planets were captured in highly eccentric orbits and remained bound to the impactor. The Jovian orbit was stationary while the terrestrial planets displayed the complex behaviour plotted in Fig. 4. We stress that these orbital histories are randomly chosen examples. Both cases showed long-term inclination oscillations between pro- and retrograde orbits, with the NS system being more regular and it also showed a larger excursion in eccentricities than the BH case. In the former, Mercury nearly circularised. In contrast, the BH planetary system had a lower bound in the eccentricity of all planets of $\geq 0.5$. In the NS case, the semi-major axes remained approximately constant for all planets while in the BH system, the terrestrial planets experienced abrupt jumps that never settled down. This may indicate the onset of longer-term chaotic behaviour. Further discussion is beyond the scope of this letter and a more extensive analysis will be a subject of a future study.

Planetary capture by a NS is particularly interesting because pulsars have been observed to possess planetary systems (even with multiple planets) – such as PSR 1257+12 (Wolszczan & Frail 1992) and PSR B1620–26 (Arzoumanian et al. 1996). While it is likely that these systems are relics (as, e.g. Wang et al. 2006), our models provide an additional formation channel – the outcome of a close encounter of a NS with an ordinary planetary system.

---

**Fig. 4.** Comparative long-term evolution of captured planetary systems. *Left:* NS: $b_{NS} = 10^{-6}$ pc, $\theta_{NS} = 90^\circ$, $v_{NS} = 50$ km s$^{-1}$. *Right:* BH: $b_{BH} = 10^{-6}$ pc, $\theta_{BH} = -15^\circ$, $v_{BH} = 10$ km s$^{-1}$. The capture event is marked by a circle for each planet. The semi-major axis of Jupiter is not plotted in the top panels, but was 11.3 au in the NS system and 24.5 au in the BH system. See text for discussion.
The mean rate for such encounters which could lead to a capture is about $3 \times 10^{-7} (n/\text{pc}^{-3}) \text{Myr}^{-1}$, where $n$ is the stellar density. For instance, this is $\gtrsim 0.03 \text{Myr}^{-1}$ in star clusters which means acquiring a planet by capture could occur within the active lifetime of a pulsar ($\lesssim 10^8$ years depending on the period).

Acknowledgements. The project was inspired by a seminar given at Pisa by E.F. Guinan, Dec. 2020. SNS thanks Matteo Cantiello, Mathieu Renzo, and Rubina Kotak for discussions regarding massive stellar evolution and supernovae. VP greatly appreciates access to computational resources supplied by the project “e-Infrastruktura CZ” (e-INFRA LM2018140) provided within the program Projects of Large Research, Development and Innovations Infrastructures. The NASA ADS, Simbad, and NASA JPL HORIZONS system were used for this research. We thank the anonymous referee for valuable comments.

References

Arzoumanian, Z., Joshi, K., Rasio, F. A., & Thorsett, S. E. 1996, in IAU Colloq. 160: Pulsars: Problems and Progress, eds. S. Johnston, M. A. Walker, & M. Bailes, ASP Conf. Ser., 105, 525
Bauermann, H., & Sollima, S. 2017, MNRAS, 472, 744
Belczynski, K., Kalogera, V., Rasio, F. A., et al. 2008, ApJS, 174, 223
Berski, F., & Dybczyński, P. A. 2016, A&A, 595, L10
Binney, J., & Tremaine, S. 2008, Galactic Dynamics: Second Edition, Princeton Series in Astrophysics (Princeton University Press)
Cai, M. X., Kouwenhoven, M. B. N., Portegies Zwart, S. F., & Spurzem, R. 2017, MNRAS, 470, 4337

Dehnen, W., & Binney, J. J. 1998, MNRAS, 298, 387
Dybczyński, P. A. 2006, A&A, 449, 1233
Famaey, B., Jorissen, A., Luri, X., et al. 2005, A&A, 430, 165
Fragione, G., Pavlík, V., & Banerjee, S. 2018, MNRAS, 480, 4955
Fryer, C. L., Belczynski, K., Wilkotowicz, G., et al. 2012, ApJ, 749, 91
Hansen, B. M. S., & Phinney, E. S. 1997, MNRAS, 291, 569
Hao, W., Kouwenhoven, M. B. N., & Spurzem, R. 2013, MNRAS, 433, 867
Harris, C. R., Millman, K. J., van der Walt, S. J., et al. 2020, Nature, 585, 357
Hege, D. C., & Hut, P. 2003, The Gravitational Million-Body Problem: A Multidisciplinary Approach to Star Cluster Dynamics (Cambridge, UK: Cambridge University Press)
Hunter, J. D. 2007, Comput. Sci. Eng., 9, 90
Jonker, P. G., & Nelemans, G. 2004, MNRAS, 354, 355
Laughlin, G., & Adams, F. C. 2000, Icarus, 145, 614
Li, G., & Adams, F. C. 2015, MNRAS, 448, 344
Malmberg, D., Davies, M. B., & Heggie, D. C. 2011, MNRAS, 411, 859
Pavlík, V., Jeřábková, T., Kroupa, P., & Baumgardt, H. 2018, A&A, 617, A69
Peuten, M., Zocchi, A., Gieles, M., Guandalis, A., & Hénaud-Brunet, V. 2016, MNRAS, 462, 2333
Rein, H., & Liu, S. F. 2012, A&A, 537, A128
Rein, H., & Spiegel, D. S. 2015, MNRAS, 446, 1424
Repetto, S., Igoshev, A. P., & Nelemans, G. 2017, MNRAS, 467, 298
Shara, M. M., Hurley, J. R., & Mardling, R. A. 2016, ApJ, 816, 59
Spurzem, R., Giersz, M., Heggie, D. C., & Lin, D. N. C. 2009, ApJ, 697, 458
Varri, A. L., Cai, M. X., Concha-Ramírez, F., et al. 2018, Comput. Astrophys. Cosmol., 5, 2
Wang, Z., Chakrabarty, D., & Kaplan, D. L. 2006, Nature, 440, 772
Wang, Y.-H., Leigh, N. W. C., Perna, R., & Shara, M. M. 2020, ApJ, 905, 136
Wolszczan, A., & Frail, D. A. 1992, Nature, 355, 145
Zheng, X., Kouwenhoven, M. B. N., & Wang, L. 2015, MNRAS, 453, 2759
Our study was initiated asking what would happen if a BH, expected to form in the Betelgeuse SN, received a kick that would direct it towards the Solar System. Exploring this required specific initial conditions linked to the progenitor and a high time resolution study. We found that the lower resolution generic cases that bounded these conditions were consistent.

For what we hereafter call ‘the Betelgeuse case’, the remnant had \( m_\odot = 10 M_\odot \) and was launched from the ecliptic latitude of the star, \(-16.627^\circ\) (J2000.0). We used this as the incidence angle in all of the high-resolution simulations. In the following discussion, we use the subscript \( \alpha \) for \( \mathrm{T} \) to label all the parameters. We used encounter velocities \( 10 \, \text{km s}^{-1} \leq v_{\alpha} \leq 190 \, \text{km s}^{-1} \). These were set up in the barycentric coordinates of the SS and, therefore, are not the actual kick velocity of \( \alpha \) Ori which has to be corrected for the stellar radial velocity (Famaey et al. 2005), that is, the kick would be \( \approx 22 \, \text{km s}^{-1} \) higher.

Our principal results are shown in Fig. A.2 and a sample realisation is shown in Fig. 1a. For \( b_\odot > 10 \, \text{pc} \), the SS remained stable regardless of \( v_\odot \) (see \( f_{\text{ret}} \)). The planetary orbits remained unchanged except for Mercury, whose inclination increased to \( 5^\circ \) (see \( \alpha_{\text{ret}}, e_{\text{ret}}, i_{\text{ret}} \)). At these distances, the \( \alpha \) Ori remnant did not significantly alter the trajectory of the SS in the Galaxy – the maximum deviation of \( 0.8 \, \text{km s}^{-1} \) (i.e. \( \approx 10 \% \) of the peculiar velocity of the Sun) was obtained for \( v_{\alpha} = 10 \, \text{km s}^{-1} \) – with a decreasing impact parameter, this effect increased (see Table A.1).

For \( 10^2 \geq b_\odot / \text{pc} \geq 10^3 \), the Sun still retained all planets if the remnant’s velocity was at least as great as the Earth’s orbital velocity. If it is very slow, \( v_\odot = 10 \, \text{km s}^{-1} \), it takes \( \approx 100 \, \text{yr} \) to traverse the SS, which is enough time to significantly alter the eccentricities of the two outermost planets. This either unbinds Neptune or results in its capture.

### Table A.1. Deviation (in absolute values) from the peculiar velocity of the Sun (Dehnen & Binney 1998), i.e. \( U \approx 10.00 \, \text{km s}^{-1} \) (towards the Galactic centre), \( V \approx 5.25 \, \text{km s}^{-1} \) (in the orbital motion of the Sun), and \( W \approx 7.17 \, \text{km s}^{-1} \) (perpendicular to the Galactic plane).

| \( v_\odot / \text{km s}^{-1} \) | \( 190 \) | \( 100 \) | \( 50 \) | \( 29 \) | \( 10 \) |
|------------------|-----|-----|-----|-----|-----|
| \( \downarrow b_\odot / \text{pc} \downarrow \text{km s}^{-1} \) | \( \Delta U \) | \( \Delta V \) | \( \Delta W \) | \( \Delta U \) | \( \Delta V \) | \( \Delta W \) | \( \Delta U \) | \( \Delta V \) | \( \Delta W \) | \( \Delta U \) | \( \Delta V \) | \( \Delta W \) |
| \( 10^{-1} \) | 0.00 | 0.00 | 0.01 | 0.01 | 0.01 |
| \( 10^{-2} \) | 0.00 | 0.00 | 0.01 | 0.02 | 0.05 |
| \( 10^{-3} \) | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| \( 10^{-4} \) | 0.02 | 0.03 | 0.06 | 0.10 | 0.32 |
| \( 10^{-5} \) | 0.04 | 0.08 | 0.16 | 0.27 | 0.80 |
| \( 10^{-6} \) | 0.00 | 0.00 | 0.00 | 0.00 | 0.03 |
| \( 10^{-4} \) | 0.15 | 0.29 | 0.61 | 1.08 | 4.77 |
| \( 10^{-5} \) | 0.42 | 0.81 | 1.61 | 2.66 | 5.78 |
| \( 10^{-6} \) | 0.00 | 0.02 | 0.01 | 0.01 | 0.20 |
| \( 10^{-4} \) | 1.58 | 3.20 | 7.86 | 16.02 | 13.50 |
| \( 10^{-5} \) | 4.25 | 7.98 | 18.44 | 18.13 | 1.01 |
| \( 10^{-6} \) | 0.04 | 0.27 | 2.07 | 7.77 | 11.40 |
| \( 10^{-3} \) | 19.23 | 47.47 | 63.19 | 40.76 | 13.00 |
| \( 10^{-4} \) | 40.43 | 57.68 | 17.15 | 4.04 | 4.28 |
| \( 10^{-5} \) | 3.83 | 21.87 | 46.66 | 34.55 | 11.90 |
| \( 10^{-6} \) | 211.61 | 136.61 | 65.98 | 39.06 | 12.90 |
| \( 10^{-3} \) | 100.80 | 9.95 | 18.65 | 12.95 | 4.61 |
| \( 10^{-4} \) | 143.42 | 114.25 | 59.49 | 35.78 | 11.90 |

For the highest velocity encounters, no planets were captured at any impact parameter above \( 10^{-6} \) pc. For all impact parameters \( b_\odot < 10^{-3} \) pc, the SS was considerably altered, especially regarding the number of planets retained and their orbital eccentricities, as shown in Fig. A.2 (\( f_{\text{ret}} \) and \( e_{\text{ret}} \)). There were no discernible effects above impact parameters \( 10^{-2} \) pc, except for the \( 10 \, \text{km s}^{-1} \) encounter velocity.

The capture cross section resulting from the simulations including the entire system is \( \Sigma_{\text{cap}} \approx 3 \times 10^{-6} \, \text{pc}^2 \), which agrees with the simple estimate from Eq. (4). The number of captured planets depended sensitively on \( v_\odot \). At \( 10 \, \text{km s}^{-1} \), all of the encounters with \( b_\odot < 10^{-3} \) pc resulted in a capture of at least one planet in more than \( 15 \% \) of the simulations. In contrast, at \( 50 \, \text{km s}^{-1} \), only \( 1/330 \) simulations resulted in the capture of a single planet (Neptune, see Fig. A.2) with the maximum cross section \( \Sigma_{\text{cap}} \approx 3 \times 10^{-4} \, \text{pc}^2 \). The number of planets captured was \( N_p \leq 7 \), all of which had high orbital eccentricities and inclinations. Regarding disruptions, at least \( 55 \% \) of the simulations with \( b_\odot < 10^{-3} \) pc resulted in the ejection of at least one planet regardless of \( v_\odot \). We stress that these values are frequencies, not probabilities, because our models are not Monte Carlo simulations. As shown in Fig. A.1, we find a scaling relation for the \( \alpha \) Ori capture cross section weighted by the frequency of models producing at least one capture of

\[
\Sigma_{\text{cap, \alpha}} \approx 7 \times 10^{-4} \left( \frac{v_\odot}{\text{km s}^{-1}} \right)^{-3.6} \, \text{pc}^2.
\] (A.1)

As a final point regarding the Betelgeuse scenario, although a disruptive encounter of its remnant with the SS is highly unlikely, even a more probable distant encounter would not be particularly pleasant. The models we present did not include any minor bodies (not even planetary moons). Their masses are negligible relative to the planets or the Sun, so they have no effect on the dynamical stability of the SS, but it is certain that the close passage of a massive body will alter their positions and velocities. We performed a few simulations with Halley-type comets (\( \alpha \approx 200 \) au), but even for an impact parameter as low as \( 10^{-2} \) pc, their orbits in the SS barycentric frame were only marginally altered. Nonetheless, a distant passage of a massive object, \( 0.1-1 \) pc, could strip away part of the Oort cloud and also produce an excess of comets with very long periods and high eccentricities that could potentially cross Earth’s orbit, as found in previous studies of stellar fly-bys (Dybczyński 2006; Berski & Dybczyński 2016).
Fig. A.2. Outcomes of the Betelgeuse scenario. For each impact parameter (coded by colours and symbols) and encounter velocity (columns), we plotted the final distribution of semi-major axes, eccentricities, and inclinations of planets that were either retained by the Sun or captured by $\alpha$ Ori (top six rows, for each planet from Mercury $\varpi$ to Neptune $\Psi$). Bottom two rows: fraction of retained and captured planets. All data were averaged over 330 simulations.
Appendix B: Additional figures: BH simulations

Fig. B.1. Capture of planets by a BH. Frequency of capture, \( f_{\text{cap}} \), of a given number of planets, \( N_p \), by the BH for the specified set of initial conditions (impact parameter, \( b_{\text{BH}} \), encounter velocity, \( v_{\text{BH}} \), and the incidence angle, \( \theta_{\text{BH}} \)).
Fig. B.2. Planet retention after a BH encounter. Frequency of retention, $f_{\text{ret}}$, of a given number of planets, $N_p$, by the Sun after the BH fly-by for the specified set of initial conditions (impact parameter, $b_{\text{BH}}$, encounter velocity, $v_{\text{BH}}$, and the incidence angle, $\theta_{\text{BH}}$).
Fig. B.3. Distribution of semi-major axes of planets captured by a BH. Each data point represents the mean value of the semi-major axis of a specific planet (Mercury \(\oplus\) to Neptune \(\oplus\)) if it was captured by a BH. The data were compiled from all pre-evolved states of the SS for a given set of initial conditions (impact parameter, \(b_{BH}\), encounter velocity, \(v_{BH}\), and the incidence angle, \(\theta_{BH}\)) – i.e. the panels do not show how many planets were captured in total (see Fig. B.1 for reference).
Fig. B.4. Distribution of semi-major axes of planets retained by the Sun after a BH encounter. Each data point represents the mean value of the semi-major axis of a specific planet (Mercury \(\oplus\) to Neptune \(\oplus\)) if it was retained by the Sun. The data were compiled from all pre-evolved states of the SS for a given set of initial conditions (impact parameter, \(b_{BH}\), encounter velocity, \(v_{BH}\), and the incidence angle, \(\theta_{BH}\)) – i.e. the panels do not show how many planets were retained in total (see Fig. B.2). The former SS is shown for reference.
Fig. B.5. Distribution of eccentricities of planets captured by a BH. Each data point represents the mean value of the eccentricity of a specific planet (Mercury ⊗ to Neptune ⊕) if it was captured by a BH. The data were compiled from all pre-evolved states of the SS for a given set of initial conditions (impact parameter, $b_{BH}$, encounter velocity, $v_{BH}$, and the incidence angle, $\theta_{BH}$) – i.e. the panels do not show how many planets were captured in total (see Fig. B.1 for reference).
Fig. B.6. Distribution of eccentricities of planets retained by the Sun after a BH encounter. Each data point represents the mean value of the eccentricity of a specific planet (Mercury \(\mathcal{M}\) to Neptune \(\mathcal{N}\)) if it was retained by the Sun. The data were compiled from all pre-evolved states of the SS for a given set of initial conditions (impact parameter, \(b_{BH}\), encounter velocity, \(v_{BH}\), and the incidence angle, \(\theta_{BH}\)) – i.e. the panels do not show how many planets were retained in total (see Fig. B.2). The former SS is shown for reference.
Fig. B.7. Distribution of inclinations of planets captured by a BH. Each data point represents the mean value of the inclination of a specific planet (Mercury to Neptune) if it was captured by a BH. The data were compiled from all pre-evolved states of the SS for a given set of initial conditions (impact parameter, $b_{BH}$, encounter velocity, $v_{BH}$, and the incidence angle, $\theta_{BH}$) – i.e. the panels do not show how many planets were captured in total (see Fig. B.1 for reference).
Fig. B.8. Distribution of inclinations of planets retained by the Sun after a BH encounter. Each data point represents the mean value of the inclination of a specific planet (Mercury \( \oplus \) to Neptune \( \Psi \)) if it was retained by the Sun. The data were compiled from all pre-evolved states of the SS for a given set of initial conditions (impact parameter, \( b_{BH} \), encounter velocity, \( v_{BH} \), and the incidence angle, \( \theta_{BH} \)) – i.e. the panels do not show how many planets were retained in total (see Fig. B.2). The former SS is shown for reference.
Appendix C: Additional figures: NS simulations

Fig. C.1. Capture of planets by a NS. Frequency of capture, $f_{\text{cap}}$, of a given number of planets, $N_p$, by the NS for the specified set of initial conditions (impact parameter, $b_{\text{NS}}$, encounter velocity, $v_{\text{NS}}$, and the incidence angle, $\theta_{\text{NS}}$).
Fig. C.2. Planet retention after a NS encounter. Frequency of retention, $f_{\text{ret}}$, of a given number of planets, $N_p$, by the Sun after the NS fly-by for the specified set of initial conditions (impact parameter, $b_{NS}$, encounter velocity, $v_{NS}$, and the incidence angle, $\theta_{NS}$).
Fig. C.3. Distribution of semi-major axes of planets captured by a NS. Each data point represents the mean value of the semi-major axis of a specific planet (Mercury to Neptune) if it was captured by a NS. The data were compiled from all pre-evolved states of the SS for a given set of initial conditions (impact parameter, $b_{NS}$, encounter velocity, $v_{NS}$, and the incidence angle, $\theta_{NS}$) – i.e. the panels do not show how many planets were captured in total (see Fig. C.1 for reference). No planets were captured in the fastest scenario.
Fig. C.4. Distribution of semi-major axes of planets retained by the Sun after a NS encounter. Each data point represents the mean value of the semi-major axis of a specific planet (Mercury \( \oplus \) to Neptune \( \mathcal{E} \)) if it was retained by the Sun. The data were compiled from all pre-evolved states of the SS for a given set of initial conditions (impact parameter, \( b_{\text{NS}} \), encounter velocity, \( v_{\text{NS}} \), and the incidence angle, \( \theta_{\text{NS}} \)) – i.e. the panels do not show how many planets were retained in total (see Fig. C.2). The former SS is shown for reference.
Fig. C.5. Distribution of eccentricities of planets captured by a NS. Each data point represents the mean value of the eccentricity of a specific planet (Mercury to Neptune) if it was captured by a NS. The data were compiled from all pre-evolved states of the SS for a given set of initial conditions (impact parameter, $b_{NS}$, encounter velocity, $v_{NS}$, and the incidence angle, $\theta_{NS}$) – i.e. the panels do not show how many planets were captured in total (see Fig. C.1 for reference). No planets were captured in the fastest scenario.
Fig. C.6. Distribution of eccentricities of planets retained by the Sun after a NS encounter. Each data point represents the mean value of the eccentricity of a specific planet (Mercury to Neptune) if it was retained by the Sun. The data were compiled from all pre-evolved states of the SS for a given set of initial conditions (impact parameter, $b_{NS}$, encounter velocity, $v_{NS}$, and the incidence angle, $\theta_{NS}$) – i.e. the panels do not show how many planets were retained in total (see Fig. C.2). The former SS is shown for reference.
**Fig. C.7.** Distribution of inclinations of planets captured by a NS. Each data point represents the mean value of the inclination of a specific planet (Mercury to Neptune) if it was captured by a NS. The data were compiled from all pre-evolved states of the SS for a given set of initial conditions (impact parameter, $b_{\text{NS}}$, encounter velocity, $v_{\text{NS}}$, and the incidence angle, $\theta_{\text{NS}}$) – i.e. the panels do not show how many planets were captured in total (see Fig. C.1 for reference). No planets were captured in the fastest scenario.
Fig. C.8. Distribution of inclinations of planets retained by the Sun after a NS encounter. Each data point represents the mean value of the inclination of a specific planet (Mercury to Neptune) if it was retained by the Sun. The data were compiled from all pre-evolved states of the SS for a given set of initial conditions (impact parameter, \(b_{\text{NS}}\), encounter velocity, \(v_{\text{NS}}\), and the incidence angle, \(\theta_{\text{NS}}\)) – i.e. the panels do not show how many planets were retained in total (see Fig. C.2). The former SS is shown for reference.