Deriving the COVID-19 Formula from any Graph

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Abstract

Most of the graphics published about the COVID-19 have exponential behavior. A lot of them have been driven with only the data given by government institutions. In this paper, the authors attempt to describe a general procedure to convert any group of data into a graph, where the application of the Least Square Method can provide a mathematical formula that can be used for different situations and purposes including improving the current graphs of the disease.

Introduction

In this article, the authors propose the use of the Least Square Method (LSM) as a procedure that can help us obtain a mathematical formula that can be used to complement, and if possible, better any of the models used so far, particularly, on the area of medicine. The LSM will be used to fit the curve of a graph from which we can generate a mathematical formula.

The procedure is a simple three-step process: first, collect the field data. Second, make a graph from the data obtained, and, as the third and last step, use the LSM to generate a mathematical formula. From the plot of this graph, after applying the LSM, we can generate a formula that can be easily taught and used worldwide without the need of having specialized workshops to teach the use and application of the formula.

Using the Least Square Method to Find the Equation of Covid-19 Curve Sample

To illustrate the proposed methodology in a step-by-step fashion, we will use a real-life example to find the equation of the curve of COVID-19 behavior. The data was obtained from a New York Time Article, The Exponential Power of Now by Siobhan Roberts [1] with the graphic of Britta Jewell [2], of the Institute for Diseasing Model.

Identifying the coordinates

The coordinates of the graph were found by measuring the height of the curve at seven different horizontal intervals, as shown in Figure 2.

Figure 1: Advert cases curve (Britta Jewell.).

Figure 2: Identification of the coordinates of the graph.
Choosing the curve's form

After determining the coordinates, it was necessary to choose a curve that approximates the shape of the COVID-19 sample curve. Figure 3 shows the graphs of some of the most commonly used functions for fitting curves using the LSM [3].

For this case, we chose the graph of the exponential function $y = ae^{bx}$ (F1) because its mirror-image, about the horizontal axis of the graph. We will use the LSM to fit the exponential graph to the profile of the curve.

System of equations

To obtain the coefficients $a$ and $b$ of the exponential function, LSM requires solving the system of equations F1 shown below. Table 1 explains the meaning of the different terms depending on the type of curve selected [4].

\[
\begin{align*}
A \sum x_i + B \sum x_i^2 &= \sum y_i \\
A \sum x_i + B \sum x_i &= \sum X_i Y_i
\end{align*}
\]

Figure 2: Samples taken at different space intervals.

Figure 3: Curves of Commonly Used functions.
Rewriting the system

Substituting the exponential values into F1 we obtain

\[ (F2) \]

Where “n” is the number of coordinates previously obtained and whose values are shown in Table 2.

### Solving the System of Equations

#### Calculating the individual terms [4]

In this example, \( n = 7 \) (the number of coordinates)

The summation of all \( X \) values is:

\[ \sum X = 0 + 7 + 14 + 21 + 28 + 35 + 42 = 147 \]

The summation of all the squares of the \( X \) coordinates is:

\[ \sum X^2 = 0 + 49 + 196 + 441 + 1225 + 1764 + 4459 = 6807 \]

The summation of the logarithms of the \( Y \) coordinates of Table 2 is:

\[ \sum \ln(y) = \ln(100) + \ln(175) + \ln(300) + \ln(575) + \ln(950) + \ln(1600) + \ln(2575) = 43.91 \]

The summation of all \( X \) coordinates multiplied by its corresponding \( Y \) logarithm is:

\[ \sum x\ln(y) = 0 \cdot 4.61 + 7 \cdot 5.16 + 14 \cdot 5.7 + 21 \cdot 6.35 + 28 \cdot 6.86 + 35 \cdot 7.38 + 42 \cdot 7.85 = 1029.4 \]

#### Substituting all terms in the System of equation F2

Performing the corresponding arithmetic operations, we obtain the following results:

\[ 7\ln(a) + 147b = 43.91 \]  
\[ 147\ln(a) + 4459b = 1029.4 \]  

(F3)

\[ 147\ln(a) + 4459b = 1029.4 \]

Calculating the b coefficient

Solving the top equation of (F3) for \( \ln(a) \) give us

\[ \ln(a) \approx \frac{43.91 - 147b}{7} \]

Replacing the value in the second equation of F3 we obtain:

\[ 147 \left( \frac{43.91 - 147b}{7} \right) + 4459b = 1029.4 \]

Solving for the coefficient \( b \) from the latter equation results in

\[ b = \frac{751.03}{9604} \approx 0.078 \]

Calculating the a coefficient

To find the coefficient \( a \), we replace the value of \( b \) in the second equation of the system F3 and solve for \( \ln(a) \). That is,

\[ 147\ln(a) + 4459(0.078) = 1029.4 \]

\[ 147\ln(a) = 1029.4 - 348.69 \]

\[ 147\ln(a) = 680.71 \]

\[ \ln a \approx 4.63 \]

Raising \( e \) to value just obtained results in:

\[ e^{\ln(a)} = e^{4.63} \rightarrow a = e^{4.63} \approx 102.6 \]

#### Equation of Covid-19’s Curve

Following the procedure outlined we can rewrite the equation 1 using the coefficients \( a \) and \( b \) just calculated

\[ a \approx 102.6 \]

\[ b \approx 0.078 \]

Using the exponential equation previously selected (F1)

\[ Y = ae^{bx} \]

and substituting the coefficients, \( a \) and \( b \) we get the following function [5]

\[ Y = 102.6e^{0.078x} \]

When we plot the latter equation into the Maple software the values of \( x \) initially obtained in Table 2, the graphic (Figure 4) obtained is very close to shape of the Figure 1. So, equation 1 approximates indeed the profile of the graphic.

### Excel Workbook Test

To improve the work we made a Microsoft Excel™ calculation spreadsheet with the LMS parameters. In the first column we placed
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Figure 5: Plot the equation obtained in Software MAPLE [6].

This EXCEL Workbook can be downloaded at the following link: http://www.escuelasuperiordeaudio.com.ve/covid19formula.html
the Xs coordinates. In the second one we can find Ys coordinates. The third column is the summation of all the Xs. The fourth column has the summation of all the squares Xs. The fifth, the summation of the logarithms of the Ys. And the sixth one, the product of each Xs by the logarithms of all the Ys.

Conclusion [7]

With the LMS method and the EXCEL Workbook propose, any person related to the study of the COVID-19 phenomenon can have a tool to predict the behavior of the disease in the time.

The authors can provide EXCEL formula translation to all who may be interested. Just email any of the authors at the email addresses indicated along the author’s names.

In addition, the Workbook can be extended to any number of samples. This obviously will help improving the accuracy of the formula.

Competing Interests

The authors declare that they have no competing interests.

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