Crosslinker mobility weakens transient polymer networks

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Transient networks comprised of polymers connected by short-lived bonds are a common design theme for both biological and synthetic materials. Transient bonds can provide mechanical rigidity, while still allowing for visco-elastic flows on timescales longer than the bond lifetime. In many biological polymer networks such as the actin cytoskeleton, the short-lived bonds are formed by accessory proteins that diffuse away after unbinding. By contrast, bonds in synthetic networks, such as the pendant groups of telechelic polymers, can only rebind in the same location. Using a recently developed theoretical model of the fracturing of visco-elastic materials, we here investigate the effect of linker mobility on the bond dynamics of a network under stress. We find that although mean field properties such as the average bond linker lifetime are barely affected by bond mobility, networks cross linked by mobile bonds fracture more readily due to 'leaking' of linkers from crack areas to less stressed regions within the network. We propose a theoretical model to describe the redistribution of mobile linkers, which we validate by simulations. Our work offers insight into a potential trade-off that cells face, between fracture strength versus the modularity and tight dynamic control offered by mobile linkers.

I. INTRODUCTION

Transient polymer networks are connected by individually short-lived bonds, which collectively result in a long-lived mechanical resistance by distributed load sharing [1]. This design principle is the basis of viscoelastic materials: the reversible bond dynamics allow the network to flow whilst maintaining mechanical integrity [2]. Furthermore, transient networks are self-healing due to the reversibility of unbinding [3] and the sensitivity of the bond dynamics to a range of external conditions makes these materials stimuli-responsive [4–6]. Due to the viscoelastic flow, transient networks are much more deformable than permanent networks [2]. However, viscoelastic materials can resist mechanical stress only for a limited time, after which the system suddenly loses its mechanical percolation, a process which is known as fracturing [3,11]. Crack initiation of viscoelastic materials occurs stochastically [1,11] due to fluctuations in the local density of bound linkers [12,13], which eventually results in fracture due to rapid crack propagation [14]. In order to understand the fracturing behavior of transient networks, one needs to understand the linker dynamics.

Transient networks can be divided in networks bound by immobile or by mobile linkers. Mobile linkers can be found in many biological systems. A well-studied example is the actin cortex, which consists of a network of actin filaments connected by actin-binding proteins [15]. These actin binding proteins can freely diffuse after unbinding. Similarly, cells use integrins [16] and cadherins [17] for cell-matrix and cell-cell adhesion [18], respectively. These adhesive proteins diffuse in the plane of the membrane after unbinding. By contrast, examples of networks connected by immobile linkers are colloidal gels connected by pendant groups [19] and adhesive polymer networks [20], such as hydrogen-bonded associative polymers [21], telechelic polymers [11], ionomers [22] and polyelectrolytes [23]. A biological example of immobile linkers can be found in fibrin blood clots, where fibrin forms fibers with pendant sticky groups which unbind upon mechanical loading [24].

Both mobile and immobile linkers result in transient networks, but only mobile linkers allow for linker re-binding in new locations of the network. This linker mobility allows for bond redistribution upon the application of mechanical stress [25,26]. Due to crack-induced stress localization [27] and subsequent force-induced linker unbinding [28], bond redistribution is most pronounced around cracks. We therefore wonder what is the effect of linker mobility on the mechanical strength of a material?

In order to investigate the effect of bond mobility on network strength, we use a model which we recently developed in the context of crack initiation in visco-elastic materials [13]. This model includes force-sensitive reversible bonds that are subjected to an external stress. Different from previous transient network models [6,28–33], this model acknowledges that the applied stress is distributed inhomogeneously over the bonds on basis of their spatial distribution [34,35]. As a result of this inhomogeneous force distribution, cracks stochastically initiate and subsequently propagate due to fluctuations in the local bond density [13]. However, this model was specific for the case of immobile linkers. We here extend the model, allowing us to include the effect of bond mobility to investigate the influence of bond mobility on the fracture strength of the network.

The main result of our work is that bond mobility hardly affects mean field properties of a bond, such as the average bound lifetime, but significantly reduces the network’s strength. We attribute the reduced network strength to the ‘leaking’ of linkers from crack areas to less stressed regions within the network. Intriguingly, mobile linkers are widespread in biology despite the reduced fracture strength compared to networks connected by immobile linkers. We speculate that cells trade frac-
ture strength for the modularity and tight dynamic control offered by mobile linkers.

II. MODEL

A. Immobile linkers

In this work, we compare a network connected by mobile linkers to a network connected by immobile linkers. For immobile linkers, we use a model that was introduced in reference [13]. Here, we briefly summarize its salient features for clarity, and afterwards explain how we extend this model to the case of mobile linkers.

We initialize a one-dimensional (1D) network with \( N \) equally spaced linkers using periodic boundary conditions, each link having a probability \( K \) to start in a bound state (figure 1a). Next we model the dynamics of the linkers with a kinetic Monte Carlo scheme [37] using the following linker dynamics:

\[
K = \frac{k_{\text{on}}}{k_{\text{on}} + k_{\text{off,0}}} \tag{1}
\]

where \( k_{\text{on}} \) is the rate of linker binding and \( k_{\text{off,0}} \) the rate of linker unbinding in the absence of force. We normalize time by the on-rate, \( k_{\text{on}} \). The off-rate increases exponentially with the applied force \( f_i \) on the linker \( i \), in keeping with the Bell model [28].

\[
k_{\text{off}}(f_i) = k_{\text{off,0}} \cdot \exp\left(\frac{f_i}{f_{1/e}}\right) \tag{2}
\]

where \( f_{1/e} \) is the force where the off-rate has decreased to \( k_{\text{off}}(f_{1/e}) = k_{\text{off,0}}/e \). We calculate the force per linker \( f_i \) via

\[
f_i = \alpha_i \cdot \sigma \tag{3}
\]

where \( \sigma \) is the stress on the system and \( \alpha \) is a yet to be defined stress intensity factor per linker. To account for the effect of inhomogeneous force distribution characteristic of polymer networks [23, 36], we assume local loading sharing. Previously, we have shown that local load sharing provides an accurate description of crack initiation in macroscopic viscoelastic materials \( (N > 100) \) [14] consistent with experiments [11, 23, 35, 39]. Specifically, we assume that the force distribution is dependent on the distance \( l_i \) of a linker to its nearest bound linker on both sides. Explicitly, we define a stress intensity factor \( \alpha \) on a bound linker at site \( i \) by:

\[
\alpha_i = N \cdot \frac{l_i}{\sum l_i} \tag{4}
\]

Note that the total force is independent of the bound fraction and normalized by the system size, \( \sum \frac{l_i}{N} = \sigma \). We normalize the applied stress by the linker force sensitivity \( f_{1/e} \). After calculating the force on all linkers, we employ a kinetic Monte Carlo step to either bind or unbind a linker stochastically. We repeat this process until all linkers are unbound, and define the time at which the last linker unbinds as the rupture time \( t_{\text{rupt}} \).

B. Mobile linkers

We model mobile linkers by initializing \( N \) linkers with a probability \( K \) to start in the bound state. Every linker gets assigned a random location in a network of length \( N \). Each bound linker follows the same unbinding rules as explained above for immobile linkers, and each unbound linker binds with a rate \( k_{\text{on}} \). However, crucially, the difference with immobile linkers is that mobile linkers get assigned a new location in the network (figure 1b), whereas immobile linkers always rebind in the same location as where they previously unbound. For mobile linkers, we consider the limit of rapid diffusion after unbinding, and therefore re-binding occurs in a random new location. Throughout the paper, we compare mobile and immobile linkers using the same parameters \( K, N \) and \( \sigma \).

III. RESULTS

To probe the mechanical strength of transient networks, we study the network lifetime as a function of the applied stress. We run 30 simulations for each set of parameters and record the rupture time as the time where the fraction of closed bonds drops to zero. This way, we compare the rupture time as a function of stress.
Strikingly, however, the mobile networks are weaker for biphasic stress-dependence of the network rupture time. Length for crack nucleation decreases (see section IV). Speeds up as a function of stress, but also the critical component with stress, but more steeply compared to the high stress regime as not only the linker unbinding is served. The average network lifetime again decreases exponentially as applied stress promotes linker unbinding. In the low stress regime, the network is metastable and linkers re-bind many times before rupturing is observed. The average network lifetime again decreases exponentially with stress, but more steeply compared to the high stress regime as not only the linker unbinding speeds up as a function of stress, but also the critical length for crack nucleation decreases (see section IV). Qualitatively, mobile and immobile linkers show a similar biphasic stress-dependence of the network rupture time. Strikingly, however, the mobile networks are weaker for all observed stresses, even though the linker affinity \( K \) and number of linkers \( N \) are identical.

To investigate why linker mobility compromises network strength, we compare the microscopic linker properties at steady state. We first consider the average lifetime of the bound linkers as a function of stress. As shown in Figure 2a, the average bound linker lifetime decreases with stress for both networks, due to force-induced unbinding. Moreover, the average lifetimes are comparable for mobile and immobile linkers. Similarly, we find that the average bond-bond distance is comparable for mobile and immobile linkers \(<l>\approx 1.4 \text{ and } <l>\approx 1.1 \text{ respectively, vertical lines in figure 2b.}\)

Why is the network lifetime with mobile linkers drastically smaller than with static linkers, even though the average linker lifetime and bond-bond distance are similar? To investigate this paradox, we need to look beyond the mean field properties as rupture is a stochastic phenomenon, initiated by the emergence and growth of cracks due to local fluctuations [11, 13, 23, 38, 39]. Plotting the distribution of bound linker distances at steady state reveals a crucial difference between immobile and mobile linkers: whereas their mean values are comparable, the bond-bond distance is significantly more widely distributed for mobile than for immobile linkers (figure 2b). We conclude that the reduced strength of networks crosslinked by mobile linkers is due to a more inhomogeneous force distribution over all bonds.

To investigate at what system size the difference between mobile and immobile linkers emerges, we compare networks with sizes ranging from \(N=1\) to \(N=10^3\) (figure 3). For both mobile and immobile linkers, \(<t_{\text{rupt}}>\) increases with \(N\) for microscopically small systems (up to \(N\approx 10\) for mobile linkers or \(N\approx 20\) for immobile linkers), as relative fluctuations in the number of bond linkers become smaller. Conversely, for macroscopically large systems (\(N\approx 30\) for mobile linkers or \(N\approx 20\) for immobile linkers) the average rupture time decreases with system size according to a power of \(-1\), as the number of crack nucleation sites increases linearly with the system size. However, an intermediate size regime exists for mobile linkers (20 < \(N\) < 30) where a faster decrease of the rupture time is observed. We hypothesize that this intermediate regime is caused by 'leaking' of linkers from stressed areas (large \(l\)) to the rest of the material.

In the limit of small systems, smaller than the crack length, re-binding of linkers always happens in the vicinity of the unbinding area. In the opposite limit of macroscopic materials, much larger than the crack length, the pool of free linkers is constant in time and therefore uncorrelated from local fluctuations in bound linker density. Thus, the network lifetime decreases solely due to the increased number of crack nucleation sites. For intermediate sized systems, there is an enhanced reduction in network lifetime with increasing system size, because the correlation between local bound linker density and pool of free linkers becomes smaller with system size. Local unbinding of a linker increases the fraction of free linkers that can subsequently rebind in the crack area. For macroscopically large systems however, the fraction of free linkers is relatively constant in time due to the rule of large numbers. In other words, linkers in macroscopic systems effectively 'leak away' from the crack area into the bulk of the material.
For macroscopic systems, \( n \) is independent of \( L \), namely \( n = n_{\text{steady}} \). We calculate \( n_{\text{steady}} \) by numerically solving:

\[
\frac{dn_{\text{steady}}}{dt} = 0 = k_{\text{on}} \cdot (N - n_{\text{steady}}) - k_{\text{off}}(\sigma) \cdot n_{\text{steady}} \tag{7}
\]

where \( k_{\text{on}} \cdot (N - n_{\text{steady}}) \) is the total rate of linker binding and \( k_{\text{off}}(\sigma) \cdot n_{\text{steady}} \) is the total rate of linker unbinding within the network. As \( k_{L+} \) increases linearly with the gap size, whereas \( k_{L-} \) increases exponentially, gaps will always become unstable for large enough \( L \) as unbinding occurs significantly more rapidly than re-binding \( L \). We are interested in the length \( L_{\text{unstable}} \) at which gaps become unstable and propagate. We approximate \( L_{\text{unstable}} \) by calculating the length at which the rate of unbinding at the edge equals the rate of binding within the center \( k_{L+}(L_{\text{unstable}}) \approx k_{L-}(L_{\text{unstable}}) \), which we can numerically solve by combining equations (6) and (7).

We test our theory quantitatively by measuring \( L_{\text{unstable}} \) by performing simulations where we ablate a gap of controlled length: first we equilibrate a network under stress until \( t = 30 \), after which we unbind all bound linkers in the positions \( l = 0 \ldots L_{\text{abl}} \). Next, we observe the network until \( t = 60 \) (figure 4b). We repeat this procedure for 100 networks per condition and plot the fraction of ruptured networks \( \phi_{\text{rupt}} \) as a function of \( L_{\text{abl}} \) (figure 4c). For small \( L_{\text{abl}} \), all networks stay intact, whereas networks become unstable and rapidly fracture for large \( L_{\text{abl}} \). We extract \( L_{\text{unstable}} \) from simulations by calculating the ablation length at which \( \phi_{\text{rupt}}(L_{\text{abl}}) = 0.5 \) via linear interpolation. We observe that mobile linkers have a shorter typical ablation length than immobile linkers (\( L_{\text{unstable}} \approx 35 \) versus \( L_{\text{unstable}} \approx 60 \), respectively (figure 4d). For both types of networks, \( L_{\text{unstable}} \) increases with \( \sigma \) as cracks are more likely to propagate under increasing stress (symbols in figure 4e). The theoretical model describes this trend correctly, although there is a systematic under-estimation of the absolute value of \( L_{\text{unstable}} \) by approximately 20\% (lines in figure 4f). A fully quantitative calculation of \( L_{\text{unstable}} \) would require solving \( \frac{dL_{\text{unstable}}}{dt} = 0 \), which is not possible as we do not have an equation for \( \frac{dL_{\text{unstable}}}{dt} \). Therefore, we have approximated the unstable point \( L_{\text{unstable}} \) by calculating the gap length at which linker unbinding is equally likely as linker binding within the gap. However, \( k_{L+}(L_{\text{unstable}}) \approx k_{L-}(L_{\text{unstable}}) \) is only a good approximation of the unstable length if an unbinding event increases the gap size by an equal amount as a re-binding event would decrease it. This assumption is not fully correct, as a linker unbinding event might only cause a marginal increase in gap length \( L \) in case the unbinding linker has a neighboring linker that is close-by, whereas a linker rebinding in the middle of the gap halves the gap size \( L \).

We next calculated the crack length \( L_{\text{unstable}} \) as a function of the bond affinity \( K \) for both mobile and immobile linkers at a fixed \( \sigma \cdot K = 0.2 \) (figure 4f). We fix \( \sigma \cdot K \) rather \( K \), because otherwise \( L_{\text{unstable}} \) would increase far
We studied the dynamics of a transient network of reversible bonds under mechanical stress, and have compared immobile linkers, which always rebind in the same place as where they unbound, with mobile linkers, which can rebind anywhere within the network. We found that the mean lifetime of bound linkers in a transient network is unaffected by the mobility of the linker (figure 2a). Yet, networks connected by mobile linkers are significantly weaker than network connected by immobile linkers, with fracturing times that are orders of magnitude lower (figure 1c). We attribute the reduced strength of networks connected by mobile linkers to the redistribution of mobile linkers from areas low in linker density, corresponding to highly stressed areas, to the rest of the material. This effect does not occur for immobile linkers, as they stay in the place from which they unbound.

Our results raise the question of why mobile linkers exist at all in nature [15–18], as immobile linkers yield stronger networks. An important thing to note in this context is that fracturing in biology is not always detrimental. In fact, fracturing in some cases is even required for biological function. For example local failure of the actin cortex can lead to cell polarization [40, 42] and facilitate a mode of cellular migration which relies on the formation of membrane blebs [43]. Similarly, destabilization and subsequent rupturing of the polar actomyosin cortex aids proper positioning of the cytokinetic furrow [44]. However, in many other circumstances fracturing of transient networks in biology is related to developmental defects [45, 46] and diseases [47, 48]. Therefore, the widespread existence of mobile linkers involved in cellular adhesion [16–18] and crosslinking of biopolymer networks [15, 49] requires explanation.

Both cell-cell and cell-matrix adhesion are mediated by proteins embedded in the membrane, which are either bound to their substrate or diffuse within the plane of the membrane and can therefore be classified as mobile linkers. Examples of such protein families are E-cadherin for cell-cell adhesion and integrin for cell-matrix adhesion [18]. The collagen matrix to which integrins adhere have mesh sizes of up to several micrometers [50], whereas the individual collagen fibers are only a few tens of nanometers thick [51]. As a result, the fraction of the membrane area which is in close enough proximity to fibers to allow for binding is very low. A large fraction of the plasma membrane area would have to be covered with immobile linkers in order to have a significant number of integrins interacting with the extracellular matrix. Instead, we speculate that linker mobility allows for diffusion through the membrane to facilitate binding to the sparse fibers. Therefore, linker mobility allows for cellular adhesion whilst requiring only a small fraction of the membrane area.

Biopolymer networks are either connected via stickiness of the fibers, for example in the case of fibrin fibers [24], or via mobile linkers such as cross linking ions which

**FIG. 4. Bond ablation for immobile and mobile linkers.** a) Kymograph representation of an ablation experiment \((K = 0.9, \sigma = 0.2, N = 10^3\) and \(l_{\text{ablate}} = 100\); mobile linkers). We plot the bond position as a function of simulation step, where white represents a bound linker and black represents an unbound linker. The first 1000 steps show steady state dynamics of stochastic binding and unbinding, after which we ablate 100 adjacent bonds. Afterwards, the ablated gap propagates and the material fractures. b) The fraction of ruptured networks \(\phi_{\text{rupt}}\) plotted as a function of ablation length \(l_{\text{ablate}}\) reveals how zones depleted of bonds can trigger fracturing. Notably, immobile linkers (red) require a larger \(l_{\text{ablate}}\) to trigger fracturing than mobile linkers (blue) \((\sigma = 0.2, K = 0.9\) and \(N = 10 \cdot l_{\text{ablate}}\). (c, d) We compare \(l_{\text{unstable}}\) from the simulations (dots) with the theoretical prediction (lines - no free parameters) as a function of the applied stress \(\sigma\) (c - fixed \(K = 0.9\)) and the bond affinity \(K\) (d - fixed \(\sigma = K = 0.2\)). Bond mobility weakens networks at high \(K\) but has no effect for small \(K\).
cross link the intermediate filament vimentin [19]. Different from the case of cellular adhesion, linker mobility does not necessarily increase the connectivity of biopolymer networks: where immobile linkers only require close proximity of two fibers, mobile linkers require the proximity of two fibers and the proximity of a linker. For ionically cross linked intermediate filaments, linkers are abundantly present as the concentration of magnesium ions in the cytosol is on the order of a µM [52]. Furthermore, as the concentration of intermediate filaments is orders of magnitude lower, in the µM regime [53], magnesium is abundant and has a low effective bond affinity K. In this regime mobile linkers are as strong as immobile linkers (figure 4d).

Another case of mobile linkers are actin binding proteins which cross link the actin cytoskeleton [15]. Many different types of cross linking proteins exist, with an enormous variety in their cross linking properties such as length [54], compliance [55], preferred binding angle [56], angular flexibility [57], typical lifetime of actin binding [58], and force sensitivity of the unbinding rate [59]. Many of these linker properties have been found to affect biopolymer network mechanics [6, 15, 54, 57, 60]. As a result, this variety of mobile linkers allows the cell to have tight dynamic control of the mechanical properties of its actin cytoskeleton, which would be difficult to obtain if the actin filaments were connected by the stickiness of the fibers.

VI. CONCLUSION

To summarize, we have studied the fracturing of transient networks connected by either mobile or immobile linkers. Our main result is that linker mobility weakens networks under stress. We have proposed and verified a theoretical model to explain this effect on basis of the leaking of linkers from crack areas to less stressed areas within the material. Even though linker mobility weakens transient networks, mobile linkers are widespread in biology. We speculate that cellular adhesion proteins are more likely to interact due to linker mobility and the large variety of mobile linkers connecting the actin cytoskeleton allows for a flexible control over the mechanics.

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