Highly Efficient and Stable Hydrogen Production in All pH Range by Two-Dimensional Structured Metal-Doped Tungsten Semicarbides

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Transition-metal-doped tungsten semicarbide nanosheets (M-doped W₂C NSs, M=Fe, Co, and Ni) have been synthesized through carburization of the mixture of tungsten trioxide, polyvinylpyrrolidone, and metal dopant. The nanosheets grow directly on the W mesh and have the lateral dimension of several hundreds of nm to a few μm with a thickness of few tens nm. It is demonstrated that the M-doped W₂C NSs exhibit superior electrocatalytic activity for hydrogen evolution reaction (HER). Impressively, the Ni-doped W₂C NSs (2 at% Ni) with the optimized HER activity show extremely low onset overpotentials of 4, 9, and 19 mV and modest Tafel slopes of 39, 51, and 87 mV dec⁻¹ in acidic (pH=0), neutral (pH=7.2), and basic (pH=14) solutions, respectively, which is close to the commercial Pt/C catalyst. Density functional theory (DFT) calculations also demonstrate that the Gibbs free energy for H adsorption of Ni-W₂C is much closer to the optimal value ΔGₜₜ = -0.073 eV as compared to -0.16 eV of W₂C. Furthermore, nearly 100% Faradaic efficiency and long-term stability are obtained in these environments. This realization of highly tolerant metal semicarbid catalyst performing on par with commercial Pt/C in all range of pH offers a key step towards industrially electrochemical water splitting.

1. Introduction

Hydrogen generated by the electrolysis of water has become an increasingly attractive energy carrier due to its high energy density [1–4]. Electrocatalysts used for the hydrogen evolution reaction (HER) are important and key components for water splitting [5, 6]. It is well known that noble metals, such as Pt, are the most efficient HER electrocatalyst due to its fast reaction kinetics and low overpotential to drive the HER reaction [7, 8]. However, its high cost and low natural abundance hamper its wide applications [9–12]. Therefore, alternative electrocatalysts with low cost, good stability, and high catalytic activity are highly desirable.

In recent years, various nonnoble metal materials, such as phosphides [13, 14], sulfides [15–19], phosphosulfides [20], and carbides [21, 22], were prepared and tested as alternatives for Pt in the HER. Among the aforementioned materials, early transition metal carbides, especially tungsten carbides [23–25] with similar d-band electronic density-of-state to that of Pt, could be considered as effective nonnoble metal HER electrocatalysts [26, 27]. For the past decades, many efforts have been devoted to the synthesis of highly active tungsten carbides (WC) HER electrocatalyst because of the above-mentioned electronic structure and other unique properties, such as high electrical conductivity, high resistance to carbon monoxide and bisulfide poisoning, and excellent corrosion tolerance over the wide range of pH and potential [28]. Unfortunately, all reported tungsten carbides (WC) exhibited poor performance towards HER. Therefore,
tungsten carbide has only been used as a catalyst support instead of carbon for Pt [24, 29].

On the other hand, tungsten semicarbide (W2C) is metal-terminated and theoretically predicted to have higher HER activity due to larger 5d-orbital electron population [30]. However, it has not been demonstrated experimentally, since the formation of W2C is not favorable below 1250°C [31]. Even at high temperature, a mixture of WC and W2C phases often forms because the metastable W2C phase is readily transformed into stable WC phase in the presence of carbon [32]. Up to date, it has been reported that W2C possesses the onset overpotential of 50 mV, which is far higher than the Pt/C benchmark (~0 mV) [33]. It may be arisen from the lack of reliable synthetic approaches. High temperature reduction (usually > 1500°C) of W or W-containing precursors by gaseous carbon source results in coking of catalyst surface and uncontrollable sintering. Consequently, it leads to lower electrochemical active surface area and then poor catalytic performance. Moreover, the morphology control and catalytic tuning should also be taken into account. As known, two-dimensional (2D) nanostructures offer good electron transfer platform, superior electron mobility, high surface area, and more surface active sites, which has not been demonstrated for W2C up to date. Therefore, it is urgent to explore an appropriate method for selective synthesis of W2C with desired 2D nanostructures and tunable electrocatalytic properties toward HER.

Herein, we report a simple strategy to prepare metal-doped W2C nanosheets (NSs) on tungsten (W) substrates at a lower synthetic temperature (900°C) through the hydrothermal reactions followed by a carburization process. The M-doped W2C NSs (M=Fe, Co, and Ni) grown directly on the W mesh, with the lateral size of several hundreds of nm to a few μm and the thickness of a few tens of nm, can be used as binder-free electrodes. This offers an efficient pathway for electron transport and the vertically aligned 2D nanostructure provides high surface area for HER. Among the M-doped W2C NSs, the Ni-doped W2C NSs (2 at% Ni) electrocatalyst exhibits close-to-Pt HER performance with low onset overpotentials of 4, 9, and 19 mV and small Tafel slopes of 39, 51, and 87 mV dec−1 in acidic (pH=0), neutral (pH=7.2), and basic (pH=14) conditions, respectively. Moreover, it gives ~100% Faradaic yield and exhibits excellent stability towards the HER in those solutions. This outstanding performance can be attributed to its optimal |ΔGₜₜₜₜ| value (close to zero) based on the density functional theory (DFT) calculations. This phase-pure W2C, with high electric conductivity, excellent tolerance, and the advantages of 2D nanostructure, would be of great interest to a wide range of research areas (i.e., electrocatalysis, Li-O₂ batteries, supercapacitor, and chemical and biological sensing), where electrical conductivity is one of the key parameters for high performance applications.

2. Results and Discussion

Scheme 1 (Supporting Information) illustrates the synthesis of M-doped W2C NSs. First, vertical growths of WO3 NSs were carried out on a W substrate by hydrothermal treatment of aqueous solution of Na₃WO₄·2H₂O and NaCl (pH ~ 2) at 180°C (Step 1). The as-obtained WO3 NSs were then immersed into a mixture of aqueous MCl₂ (MCl₂=FeCl₂, CoCl₂, and NiCl₂) dopant and polyvinylpyrrolidone (PVP) precursor, followed by heat treatment at 180°C to obtain the WO3/PVP/M mixture (Step 2). Finally, the as-prepared WO3/PVP/M mixture was carburized at 900°C under the H₂/Ar environment to obtain the M-doped W2C NSs (Step 3).

In Figure 1(a), the X-ray diffraction (XRD) peaks located at 40.2, 58.2, and 73.2° correspond to the W substrate (ICPDS No. 04-0806). After growth of WO3 NSs on the W substrate, all the XRD peaks (Figure S1, Supporting Information) can be indexed to the hexagonal WO3 (ICPDS No.33-1387) and W (ICPDS No. 04-0806). After carburization, the XRD peaks (Figure 1(a)) match those of W2C (ICPDS No. 35-0776) with space group of P-3m1 (a = 0.30387 nm and c = 0.46528 nm) and W (ICPDS No. 04-0806). Moreover, M-doped W2C (M=Fe, Co, and Ni) samples with varied dopant content have also been prepared. The amount of metal dopants was determined by the inductively coupled plasma-optical emission spectroscopy (ICP-OES, Table S1, Supporting Information). Due to the difference in ionic sizes and ionic charges we can only dope up to 4 at% of M into W2C lattice and 2 at% M-doped W2C (namely, 2% M-W2C, M=Fe, Co, and Ni) was mainly used for detail characterizations. It is notable that the (110) peak of W (40.2°) overlaps with the (101) peak of W2C (39.6°). Therefore, to obtain accurate lattice constants for 2% M-W2C, the nanosheets were scrapped off from the W mesh and dropped cast onto Cu substrate, and the XRD peaks were calibrated with the crystalline Cu (ICPDS No. 04-0836) as an internal standard (Figure 1(b)). The XRD patterns of M-W2C (M=Fe, Co, and Ni) with varied doping content (0–4%) reveal that the diffraction peaks of (100), (002), and (101) at 34.5°, 38.0°, and 39.6°, respectively, slightly shift to the higher angles as compared to those of pure W2C (Figures 2(a)–2(d); Figures S2a–S2d and S3a–S3d in Supporting Information). It is worth noting that Cu as the internal reference did not show any detectable peak shift in the XRD measurements; hence, this kind of peak shift indicates the decrease of lattice parameters (i.e., a and c as shown in Figure S4 in Supporting Information) after M (M=Fe, Co, and Ni) was doped into the W2C lattice. To specify, the Rietveld refinement method [34] was performed to determine the changes of lattice parameters and the unit cell volumes with respect to the amount of dopant. The lattice parameters and consequently the unit cell volume decrease with the increased dopant content, implying that smaller Ni, Co, or Fe atoms have substituted for the W atoms randomly in the crystal structure (Figures 2(e)–2(g); Figures S2e–S2g and S3e–S3g in Supporting Information). Such observation is expected as the Ni, Co, and Fe atoms have smaller radii as compared to W [35].

The X-ray photon-electron spectroscopy (XPS) was also used to characterize the 2% M-W2C (M=Fe, Co, and Ni) (Figure 1(c)). The two strong peaks at 853.3 eV and 869.9 eV with two corresponding satellite peaks in the Ni 2p XPS spectrum can be assigned to the Ni²⁺ in Ni-C bond, which are
the characteristic of Ni-doping in metal carbide materials [36, 37]. In the fine Co 2p XPS spectrum, peaks at binding energies of 778.4 eV and 793.4 eV and their satellites correspond to Co 2p3/2 and Co 2p1/2, indicating the presence of Co2+ and Co3+ in Co-C bond [37]. The peaks at 707.0 eV and 720.1 eV in the Fe 2p XPS spectrum are attributed to Fe2+ in Fe-C bond [37, 38]. All these results suggest that the Fe, Co, and Ni have been successfully doped into W2C.

The scanning electron microscopy (SEM) images of W2C and 2% M-W2C (M=Fe, Co, and Ni) samples (Figures 3(a) and 3(b) and Figures S3a and S3b in Supporting Information) clearly show that the individual nanosheets were densely grown on the W mesh. The thickness of the whole nanosheet film on W mesh is ~1.0 μm (Figure S6, Supporting Information). The obtained W2C and 2% M-W2C nanosheets were then scraped off from the W mesh for the atomic force microscopy (AFM), transmission electron microscopy (TEM), and high-resolution (HR) TEM measurements. The AFM result confirmed that the thickness of the nanosheet is several tens of nm (Figure S7, Supporting Information). As shown in the TEM images (Figures 3(c) and 3(d)), the shape of the NSs is irregular and the lateral dimension of the nanosheets is from several hundreds of nm to a few μm. The HRTEM image of W2C nanosheet shows a lattice spacing of 0.260 nm (Figure 3(e)), corresponding to the d-spacing of (010) atomic planes of the W2C phase, whereas those lattice fringes for 2% M-W2C (M=Fe, Co, and Ni) are slightly higher at 0.261 nm (Figure 3(f) and Figures S5c and S5d), which is in a good agreement with the peak shift seen in XRD patterns. The selected area electron diffraction (SAED) patterns (insets in Figures 3(e) and 3(f) and Figures S5c and S5d in Supporting Information) show the single crystalline nature of the observed W2C and 2% M-W2C NSs (M=Fe, Co, and Ni) with exposure of (001) facets. The high-angle annular dark field (HAADF) images and scanning transmission electron microscopes-energy dispersive X-ray spectroscopy (STEM-EDX) mapping images (Figure S8, Supporting Information) prove that W, C, and the doped metals are uniformly distributed over the 2% M-W2C NSs (M=Fe, Co, and Ni).

Figure 1: XRD and XPS characterizations of various metal dopants in W2C NSs. (a) XRD patterns of W substrate, W2C, and 2% M-W2C NSs (M=Fe, Co, and Ni) on W substrate. (b) XRD patterns of Cu internal standard, W2C, and 2% M-W2C NSs (M=Fe, Co, and Ni) using Cu as internal standard. (c) High-resolution XPS spectra of Fe 2p, Co 2p, and Ni 2p for 2% M-W2C NSs (M=Fe, Co, and Ni).
Figure 2: XRD analyses of various doping contents in M-W$_2$C NSs. (a) XRD patterns and (b, c) magnified XRD patterns of W$_2$C and W$_2$C with various Ni (at%) doping contents. (d) Magnified XRD patterns of W$_2$C and W$_2$C with various Ni (at%) doping contents using Cu as internal standard. (e, f) The plots of lattice parameters a and c versus Ni (at%) doping content measured by ICP-OES. (g) The plot of unit cell volume of W$_2$C versus Ni (at%) doping content measured by ICP-OES.
are 145, 102, 122, and 39 mV dec\(^{-1}\) for the pure W\(_2\)C, 2% Fe-W\(_2\)C, 2% Co-W\(_2\)C, and 2% Ni-W\(_2\)C NSs, respectively (Figure 4(c)). It means that the HER for pure W\(_2\)C, 2% Fe-W\(_2\)C, and 2% Co-W\(_2\)C proceeds through the Volmer-Heyrovsky mechanism, in which the Volmer reaction is the rate-limiting step [39], whereas the HER for 2% Ni-W\(_2\)C NSs follows the Volmer-Tafel reaction process, in which the recombination of adsorbed hydrogen atoms is the rate-determining step [39]. Notably, the Tafel slope of 2% Ni-W\(_2\)C NSs is close to the commercial 20% Pt/C electrocatalyst...
(30 mV dec$^{-1}$), suggesting that 2% Ni-W$_2$C NS electrode might be used to replace the expensive Pt electrocatalyst for HER. The inherent activities toward HER were also evaluated by the exchange current density. The 2% Ni-W$_2$C still performs well at 0.79 mA cm$^{-2}$, which is far higher than W$_2$C (0.19 mA cm$^{-2}$), 2% Fe-W$_2$C (0.22 mA cm$^{-2}$), and 2% Co-W$_2$C (0.41 mA cm$^{-2}$) and is just slightly below Pt/C (0.92 mA cm$^{-2}$).

In light of the high electrocatalytic activity of 2% M-W$_2$C NSs (M=Fe, Co, and Ni), the electrochemical effective surface area (ESCA), which is proportional to the measured double-layer capacitance ($C_{dl}$), was determined using cyclic voltammetry (Figures 5(a)–5(d)). The $C_{dl}$ values of the W$_2$C, 2% Fe-W$_2$C, 2% Co-W$_2$C, and 2% Ni-W$_2$C electrodes are 38, 54, 58, and 75 mF cm$^{-2}$, respectively (Figure 5(e)). The 2- to 2.5-fold higher ESCA of 2% M-W$_2$C NSs as compared to the pure W$_2$C indicates that the number of surface active sites significantly increased after the substitutional doping of transition metal atom (e.g., Fe, Co, or Ni) in W$_2$C NSs. Importantly, after ECSA normalization, the HER activity of 2% Ni-W$_2$C NSs is still the best (Figure 5(f)). Hence, the enhancement seen in HER activity is attributed not only to the increase of ECSA but also to the high intrinsic activity of 2% M-W$_2$C NSs, especially 2% Ni-W$_2$C NSs. Electrochemical impedance spectroscopy (EIS) results (Figure S11, Supporting Information) compare the charge transfer resistance ($R_{ct}$) of pure W$_2$C and 2% M-W$_2$C (M=Fe, Co, and Ni) electrodes. The obtained $R_{ct}$ values of pure W$_2$C, 2% Fe-W$_2$C, 2% Co-W$_2$C, and 2% Ni-W$_2$C are 43.8 Ω, 29.0 Ω, 25.7 Ω, and 12.6 Ω, respectively. The lowest $R_{ct}$ of 2% Ni-W$_2$C could be attributed to the fast reaction rate for the proton reduction on the electrocatalyst surface.
Figure 5: ECSA analysis. Cyclic voltammograms (CVs) of (a) W$_2$C, (b) 2% Fe-W$_2$C, (c) 2% Co-W$_2$C, and (d) 2% Ni-W$_2$C NSs obtained in a potential window of 0.192–0.242 V (vs. RHE) at various scan rates of 5, 10, 20, 50, and 100 mV s$^{-1}$ in 0.5 M H$_2$SO$_4$ solution. (e) The capacitive current ($j_{\text{anodic}} - j_{\text{cathodic}}$) at 0.22 V (vs. RHE) as a function of the scan rate for the W$_2$C and 2% M-W$_2$C (M=Fe, Co, or Ni) NSs. (f) HER polarization curves of W$_2$C, 2% Fe-W$_2$C, 2% Co-W$_2$C, and 2% Ni-W$_2$C NSs after electrochemical active area (ECSA) normalization.
Due to the best performance of 2% Ni-W₂C in acidic condition, it is necessary to evaluate its long-term durability. Continuous CV was performed between 0.2 and -0.3 V (vs. RHE) at a scan rate of 100 mV s⁻¹ in 0.5 M H₂SO₄ solution (Figure 4(d)). As can be seen, the polarization curves before and after 1000 CV cycles almost overlap with each other. Chronoamperometry measurement of 2% Ni-W₂C NSs at overpotential of 180 mV also shows a stable current density of 108 mA cm⁻² for 28 hours (Figure 4(d), inset). The post HER analysis, i.e., XRD, XPS, and SEM (Figures S12a, S13a, S14a, and Table S1 in Supporting Information), shows almost no change observed, revealing high structural and chemical stability. All these results suggest the remarkable stability and durability of the synthesized 2% Ni-W₂C NSs in such HER process.

An ideal HER electrocatalyst should not only have comparable activity/efficiency to Pt/C in 0.5 M H₂SO₄, but also acquire high catalytic activity and good stability over a wide pH range. Therefore, we further examine the electrochemical performance of the 2% M-W₂C NSs (M=Fe, Co, and Ni) in neutral (1 M phosphate buffer, pH=7.2) and basic (1 M KOH, pH=14) solutions. In neutral condition, the reductive sweep of W₂C reveals a high η₁₀ of 334 mV for HER (Figure 6(a)). In contrast, noticeable enhancement was obtained with lower η₁₀ (242 mV, 188 mV, and 63 mV for 2% Fe-W₂C, 2% Co-W₂C, and 2% Ni-W₂C, respectively) and sharply increased cathodic current. Interestingly, the 2% Ni-W₂C still displays favorable performance, which is further shown by its modest onset overpotential and Tafel slope of 9 mV and 51 mV dec⁻¹, respectively (Figure 6(b)), while the values for W₂C, 2% Co-W₂C, and 2% Fe-W₂C are less attractive at 227 mV and 143 mV dec⁻¹; 67 mV and 96 mV dec⁻¹; 123 mV and 98 mV dec⁻¹, respectively. Similarly, HER catalytic activity in basic condition is presented in Figures 6(d) and 6(e). The onset overpotential and η₁₀ for 2% Ni-W₂C are 19 mV and 81 mV, respectively, surpassing the 2% Co-W₂C (85 mV and 213 mV), 2% Fe-W₂C (188 mV and 312 mV), and W₂C (226 mV and 380 mV) by a great margin. The Tafel slope for 2% Ni-W₂C in KOH solution is 87 mV dec⁻¹, which is slightly worse than that of the commercial 20% Pt/C (60 mV dec⁻¹) and is much lower than those of 2% Co-W₂C (130 mV dec⁻¹), 2% Fe-W₂C (102 mV dec⁻¹), and W₂C (133 mV dec⁻¹). Furthermore, these values of 2% Ni-W₂C are much better than the reported electrocatalysts (Tables S3–S7, Supporting Information).

The stability and durability of 2% Ni-W₂C in PBS and KOH solution were also investigated by continuous CV and chronoamperometry method (Figures 6(c) and 6(f)). Less than 5% changes in current density are observed within 28 hours of electrolysis at 180 mV overpotential in both solutions. After 1000 CV scans, the reductive sweep voltammograms shows a slight negative shift compared to the initial one (Figures 6(c)–6(f), inset). In addition, the SEM results for 2% Ni-W₂C after the durability test indicate no obvious changes in the 2D morphology (Figures S12b and S12c, Supporting Information). Similarly, the XRD patterns (Figures S13b and S13c, Supporting Information) of the 2% Ni-W₂C NSs samples after chronoamperometry measurements for 28 h, specifically the diffraction peaks at 34.5°, 38.0°, and 39.6° corresponding to (100), (002), and (101) planes, respectively, resemble those of the W₂C (ICPDS 35-0776) in acidic, neutral, and alkaline solutions. These detectable peaks indicate that the phases of the samples remain unchanged after long-term HER testing. Equally important, Figures S14b and S14c in Supporting Information show the binding energies of the 2% Ni-W₂C NSs samples at 853.3 eV (Ni 2p₁/₂) and 869.9 eV (Ni 2p₃/₂) which are attributed to the Ni dopant in the W₂C phase. These noticeable peaks imply that the chemical structures of Ni dopant in the W₂C structure remain unchanged after durability test for 28 h in various pH solutions. On top of that, quantitative XPS analyses show almost no nickel leaching (Table S1, Supporting Information). Those results demonstrate that the 2% Ni-W₂C possesses remarkable stability in HER under neutral and basic condition, suggesting the promise for implementing this new catalyst into realistic cathodic electrode for water splitting.

Faradaic efficiency tests in the pH solutions of 0, 7.2, and 14 were also conducted (Figure S15, Supporting Information). For experimental amount of H₂ generated, headspace samples were taken for gas chromatography every 20 minutes while operating continuously at ~80 mA cm⁻². The theoretical volume of H₂ evolved was calculated by Faraday’s law with the assumption that all electrons passing through the circuit engage in proton reduction. The experimental and theoretical amounts of H₂ generated are in a good agreement, showing almost 100% current to hydrogen productivity.

To understand the effect of the Ni dopant in W₂C toward the HER activity, a systematic calculation on the electronic properties of pure W₂C and Ni-W₂C was carried out by employing DFT calculations (details of simulation method can be seen in the experimental section in Supporting Information). The proposed surface active sites of the Ni-W₂C were then theoretically predicted by the HER free energy diagrams. The overall HER pathway can be described by a three-state diagram: (1) an initial state (H⁺ + e⁻), (2) an intermediate state (adsorbed H*), and (3) a final state (1/2 H₂ product) [7]. As known, the optimal value of Gibbs free energy of H* adsorption, |ΔG_H*,| should be zero, leading to the optimal HER electrocatalytic activity. Negative ΔG_H* implies that the desorption of H* is to be the rate-determining step (RDS), while positive ΔG_H* means that the formation of intermediate H* is the RDS [7]. As shown in Figure 7(a), there are three possible adsorption sites for hydrogen on W₂C nanosheet, i.e., the top of W atom (T), two trigonal sites with superimposing with C (H1), and bottom W atoms (H2). Based on the calculations, H prefers to be adsorbed at the H2 sites with lowest free energy of -0.71 eV (Table S8, Supporting Information). With Ni doping, we firstly investigated the energy-preferable adsorption site out of 4 H2 sites in the configuration (sites 1-4 in Figure 7(a)). As shown in Figure 7(b), the H adsorbed on site 4, which is far away from the doping position, has the lowest free energy. This reveals that the H will be preferable to be adsorbed firstly on the sites away from the doping position. Therefore, at high hydrogen adsorption coverage, the sites far away from the doping position are preferably occupied by hydrogen.
Figure 6: HER electrochemical performances in neutral and alkaline condition. (a-c) 1 M PBS (pH=7.2) and (d-f) 1 M KOH (pH=14) solutions. (a, d) Polarization curves of the 20% Pt/C, W$_2$C, 2% Fe-W$_2$C, 2% Co-W$_2$C, and 2% Ni-W$_2$C NSs and their corresponding (b, e) Tafel plots. (c, f) Polarization curves of 2% Ni-W$_2$C NSs before and after 1000 cyclic voltammetry cycles (Inset: chronoamperometry measurements at overpotential of 180 mV).
3. Conclusion

In summary, we have successfully synthesized M-W$_2$C NSs (M=Fe, Co, and Ni) on W meshes. The M-W$_2$C NSs electrocatalysts show remarkable HER activities. Particularly the 2% Ni-W$_2$C NSs exhibit low onset overpotentials of 4 mV, 9 mV, and 19 mV alongside with modest Tafel slopes of 39 mV dec$^{-1}$, 51 mV dec$^{-1}$, and 87 mV dec$^{-1}$ in acidic (0.5 M H$_2$SO$_4$, pH=0), neutral (1M PBS, pH=7.2), and basic (1M KOH, pH=14) solutions, respectively. Importantly, the 2% Ni-W$_2$C exhibits excellent Faradaic efficiency and long-cycling stability in those environments. DFT calculations further confirm the effectiveness of Ni incorporation by reducing $\Delta G_{\text{H}^+}$ significantly from 0.16 eV of W$_2$C to 0.073 eV of Ni-W$_2$C. This realization of nonnoble metal binder-free electrode with high tolerance and close-to-Pt electrocatalytic activity in a wide range of pH makes 2% Ni-W$_2$C a promising contender for future development of H$_2$ generation via electrochemical water splitting.

4. Materials and Methods

4.1. Growth of WO$_3$ NSs on W Mesh. Firstly, the WO$_3$ NSs were grown on the tungsten substrate using the hydrothermal method. Tungsten substrate was cleaned by sonication in a mixture of deionized water and ethanol (1:1 v/v ratio) for 15 min followed by drying at 50°C in vacuum oven. In a typical process, 0.4 mmol of Na$_2$WO$_4$.2H$_2$O (Sigma-Aldrich) and 3.4 mmol of NaCl (Sigma-Aldrich) were dissolved in 6 mL of deionized water. Then 4.0 M of HCl (Merck, USA) aqueous solution was added dropwise to adjust the pH to 2.0. The solution obtained was transferred to a 23-mL Teflon-lined stainless-steel autoclave where the reaction was maintained at 180°C for 5 h. The synthesized WO$_3$ NSs electrode was then washed sequentially with deionized water and ethanol and then dried in an oven at 50°C.

4.2. Synthesis of M-W$_2$C NSs. In a typical synthetic procedure of W$_2$C NSs, a mass ratio of polyvinylpyrrolidone (PVP, average mol wt 40,000) to WO$_3$ NSs (40:1) was homogeneously
mixed in 4 mL of deionized water. For M-W₂C synthesis, various M dopants (i.e., FeCl₃, CoCl₂, and NiCl₂, Sigma-Aldrich) were also added to the solution mixture. The amount of M dopants and W contents in the M-W₂C samples was determined by energy-dispersive X-ray spectroscopy (EDX), elemental mapping, and high angle annular dark field scanning transmission electron microscopy (HAADF-STEM) were performed by using a Tecnai G2 F20 S-TWIN (JEOL, Model JEM-2100F, 2010 UHR; JEM-ARM200F) operating at 200 keV, field emission scanning electron microscopy (FESEM, JEOL, JSM-7600F), and atomic force microscopy with scanning transmission electron microscopy (AFM) (Digital Instruments). The energy-dispersive X-ray spectroscopy (EDX), elemental mapping, and high angle annular dark field scanning transmission electron microscopy (HAADF-STEM) were performed by using Dual-view Optima 5300 DV ICP-OES. Rietveld refinement method was processed using the TOPAS software. The X-ray photoelectron spectroscopy (XPS, Kratos AXIS Supra) spectra were conducted using Al anode.

4.3. Materials Characterization. X-ray diffraction was performed to characterize the sample on the Shimadzu XRD-6000 X-ray diffractometer with Cu-Kα irradiation (λ = 1.5406 Å). The morphology and structure of the materials were characterized using transmission electron microscopy with scanning transmission electron microscopy (JEOL, Model JEM-2100F, 2010 UHR; JEM-ARM200F) operating at 200 keV, field emission scanning electron microscopy (FESEM, JEOL, JSM-7600F), and atomic force microscopy (AFM) (Digital Instruments). The energy-dispersive X-ray spectroscopy (EDX), elemental mapping, and high angle annular dark field scanning transmission electron microscopy (HAADF-STEM) were performed by using Dual-view Optima 5300 DV ICP-OES. Rietveld refinement method was processed using the TOPAS software. The X-ray photoelectron spectroscopy (XPS, Kratos AXIS Supra) spectra were conducted using Al anode.

4.4. Electrochemical Measurement. Electrochemical measurements were performed in a conventional three-electrode system using graphite rod as the counter electrode and the as-synthesized M-W₂C, W₂C NSs on W substrate as working electrode. Satured calomel electrode served as the reference electrode in acidic and neutral solutions while Hg/HgO served as the reference electrode in basic solution. For comparison, 20% Pt/C catalyst slurry in IPA/Nafion mixture (0.95/0.05 v/v ratio) was drop-casted on W substrate and used as working electrode. Doctor blade was also employed to make sure the catalyst loadings are at 1 mg cm⁻². All measurements were carried out in H₂-purged 0.5 M H₂SO₄ (pH=0), 1 M phosphate buffer (pH=7.2), and 1 M KOH (pH=14) electrolytes. For the linear sweep voltammetry (LSV) measurements, the scan rates were set to be 2 mV s⁻¹ to minimize the capacitive current. All the potentials were calibrated to a reversible hydrogen electrode (RHE) by using the following equations:

\[ E_{RHE} = E_{SCE} + 0.059 \times \text{pH} + E_{SCE}^o \]

(1)

where \( E_{SCE}^o = 0.241 \) V.

\[ E_{RHE} = E_{Hg/HgO} + 0.059 \times \text{pH} + E_{Hg/HgO}^o \]

(2)

where \( E_{Hg/HgO}^o = 0.098 \) V.

All HER results were corrected for all ohmic (IR) losses throughout the system. To obtain the ohmic resistance, the electrochemical impedance spectroscopy (EIS) measurements were performed with frequency from 0.1 Hz to 100 Hz at an amplitude of 10 mV. The electrochemical surface area (ESCA) was estimated from the double-layer capacitance (Cdl) of the films. The Cdl was determined with a simple cyclic voltammetry (CV) method. The CV was conducted in a potential window (0.192-0.242 V vs. RHE) at various scan rates of 5, 10, 20, 50, and 100 mV s⁻¹. Then capacitive current (i_anodic - i_cathodic) at 0.22 V vs RHE was plotted against various scan rates, while the slope obtained was divided by two to obtain the Cdl value. The Faradaic efficiency of the catalysts was determined by passing 80 mA cm⁻² of current density through the water electrolysis system and the hydrogen gas generated was determined by analyzing 500 μL of headspace samples via gas chromatography. The Faradaic efficiency is then defined as the ratio of the measured amount of H₂ to that of the theoretical amount of H₂ (based on Faraday’s law).

4.5. Simulation Details and Methods. All the calculations were performed by using density functional theory (DFT) as implemented in the Vienna ab initio package (VASP) [40]. The projector augmented wave (PAW) method [41] was used to describe electron-ion interaction, while the generalized gradient approximation using the Perdew-Burke-Ernzerhof (PBE) functional was used to describe the electron-exchange-correlation. A plane wave basis was set up to an energy cutoff of 520 eV. A 4 x 4 x 1 k-grid was used to investigate the adsorption of hydrogen. A 30 Å vacuum space was constructed to avoid the periodical image interactions between periodical interactions. The Brillouin zone was integrated using the Monkhorst-Pack scheme [42] with 3 x 3 x 1 k-grid. All the atomic positions and cell parameters were relaxed using a conjugate gradient minimization until the force on each atom is less than 0.01 eV Å⁻¹.

Gibbs free-energy of the H adsorption was calculated using equation (2):

\[ \Delta G_H = \Delta E_H + \Delta E_{ZPE} - T\Delta S_H \]

(2)

where \( \Delta E_{ZPE} \) and \( \Delta S_H \) are the zero-point energy and entropy difference of hydrogen in the adsorbed state and the gas phase, respectively. The hydrogen adsorption energy \( \Delta E_H \) is calculated by the following expression:

\[ \Delta E_H = E_{Ni+nH} - E_{Ni+(n-1)H} - \frac{1}{2}E_{H_2} \]

(3)

where \( E_{Ni+nH} \) and \( E_{Ni+(n-1)H} \) are the total energy of Ni-W₂C nanosheet with n-th and (n-1)-th H atoms adsorption, respectively. \( E_{H_2} \) is the energy of a gas-phase hydrogen molecule.
The calculated frequency of H$_2$ gas is 4345 cm$^{-1}$. The contribution from the configurational entropy in the adsorbed state is small and neglected. So the entropy of hydrogen adsorption as $\Delta S_{H_2} = (1/2)S_{H_2}$, where $S_{H_2}$ is the entropy of molecule hydrogen in the gas phase at standard conditions. With these values, the Gibbs free energy from equation (2) can be rewritten as

$$\Delta G_{H_2} = \Delta E_{H_2} + 0.29$$

(4)

Data Availability

All data generated or analyzed during this study are included in this published article and its Supplementary Materials.

Conflicts of Interest

The authors declare no competing financial interests.

Authors’ Contributions

Wei Huang, Hua Zhang, and Qingyu Yan received and coordinated the project. Edison H. Ang and Khang N. Dinh designed the experiments. Edison H. Ang and Khang N. Dinh synthesized and performed material characterizations. Ying Huang performed AFM and TEM measurements. Zhili Dong performed the XRD and Rietveld refinement. Jun Yang and Xiaochen Dong evaluated the electrochemical performances. Xiaoli Sun and Zhiguo Wang performed the simulation. Xiaolin Sun and Zhiqiao Wang performed the simulation. Edison H. Ang and Khang N. Dinh wrote the paper. All authors contributed to the discussion. Edison H. Ang and Khang N. Dinh contributed equally to this work.

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Supplementary Materials

Scheme 1: schematic diagram illustrating the growth process of M-W$\text{CO}_3$ NSs (M=Fe, Co, and Ni) on W substrate. Step 1: growth of WO$_3$ NSs on W substrate. Step 2: growth of the WO$_3$/PVP/M on the presynthesized WO$_3$ NSs. Step 3: formation of M-W$\text{CO}_3$ NSs by carburing the WO$_3$/PVP/M NSs for HER. Figure S1: XRD pattern of WO$_3$ NSs on W substrate. Figure S2: (a) XRD patterns, (b, c) magnified XRD patterns of W$_2$C and W$_2$C with various Fe (at%) doping contents, (d) magnified XRD patterns of W$_2$C and W$_2$C with various Fe (at%) doping contents using Cu as internal standard, (e, f) the plots of lattice parameters a and c versus Fe (at%) doping content measured by ICP-OES, and (g) the plot of unit cell volume of W$_2$C versus the Fe (at%) doping content measured by ICP-OES. Figure S3: (a) XRD patterns, (b, c) magnified XRD patterns of W$_2$C and W$_2$C with various Co (at%) doping contents, (d) magnified XRD patterns of W$_2$C and W$_2$C with various Co (at%) doping contents using Cu as internal standard, (e, f) the plots of lattice parameters a and c versus Co (at%) doping content measured by ICP-OES, and (g) the plot of unit cell volume of W$_2$C versus Co (at%) doping content measured by ICP-OES. Figure S4: schematic representation of the crystal structure of hexagonal W$_2$C with a space group of P-3m1. Figure S5: SEM and TEM characterizations of (a, c) 2% Fe-W$_2$C and (b, d) 2% Co-W$_2$C NSs, (a, b) FESEM images, and (c, d) HRTEM images (insets: corresponding SAED patterns). Figure S6: SEM image of the cross-section view of pure W$_2$C NSs on W substrate. Figure S7: AFM image of pure W$_2$C NSs and the corresponding height profile along the white dashed line. Figure S8: HAADF images and their corresponding STEM-EDX mapping images of (a-d) 2% Fe-W$_2$C, (e-h) 2% Co-W$_2$C, and (i-l) 2% Ni-W$_2$C NSs. Figure S9: polarization curve of W substrate at the scan rate of 2 mV s$^{-1}$ in 0.5 M H$_2$SO$_4$ solution. Figure S10: polarization curves of M-W$_2$C electrodes (M=Fe, Co, and Fe) with varied (a) Ni, (b, c) Co, and (d) Fe contents. The content of M in the W$_2$C lattice was determined by using ICP-OES elemental analysis. The measurements were conducted at the scan rate of 2 mV s$^{-1}$ in 0.5 M H$_2$SO$_4$ solution (pH=0). Figure S11: Nyquist plots of W$_2$C and 2% M-W$_2$C (M=Fe, Co, and Ni) NSs. The EIS measurements were recorded at amplitude of 10 mV in 0.5 M H$_2$SO$_4$ solution. Inset: Randles circuit model, where R$_e$ represents series resistance, C$_{dl}$ represents double-layer capacitance, and R$_ct$ represents the charge transfer resistance at the electrode-electrolyte interface. Figure S12: SEM images of 2% Ni-W$_2$C NSs after chronoamperometry measurements for 28 h in (a) 0.5 M H$_2$SO$_4$ (pH = 0), (b) 0.1M PBS (pH = 7.2), and (c) 1M KOH (pH = 14). Figure S13: XRD patterns of 2% Ni-W$_2$C NSs samples after chronoamperometry measurements for 28 h in (a) 0.5 M H$_2$SO$_4$ (pH = 0), (b) 1 M PBS (pH = 7.2), and (c) 1 M KOH (pH = 14). Figure S14: Ni 2p XPS spectrums of 2% Ni-W$_2$C NSs after chronoamperometry measurements for 28 h in (a) 0.5 M H$_2$SO$_4$ (pH = 0), (b) 1 M PBS (pH=7.2), and (c) 1 M KOH (pH = 14). Figure S15: Faradaic efficiency of hydrogen generation measured within 300 min on 2% Ni-W$_2$C NSs after chronoamperometry measurements at current density of 80 mA cm$^{-2}$ in (a, b) 0.5 M H$_2$SO$_4$ (pH = 0), (c, d) 1M PBS (pH = 7.2), and (e, f) 1 M KOH (pH = 14). Table S1: composition analysis of the M-W$_2$C (M= Fe, Co, and Ni) by ICP-OES and XPS. Table S2: onset overpotentials, operating overpotentials at current density $j=10$ mA cm$^{-2}$. Tafel slopes, and exchange current densities of different samples obtained in 0.5 M H$_2$SO$_4$ solution. The amount of metal dopant was kept at 2 at% for all the M-W$_2$C NSs. Table S3: HER performances of the 2% Ni-W$_2$C electrocatalyst in this study in comparison to various types...
of phosphide electrocatalysts in the literature. Table S4: HER performances of the 2% Ni-W2C electrocatalyst in this study in comparison to various types of sulfide electrocatalysts in the literature. Table S5: HER performances of the 2% Ni-W2C electrocatalyst in this study in comparison to various types of carbide electrocatalysts in the literature. Table S6: HER performances of the 2% Ni-W2C electrocatalyst in this study in comparison to various types of the reported electrocatalysts used in the neutral electrolyte. Table S8: free energies of hydrogen adsorption to 3 are the possible adsorption sites (T, H1, and H2) on W2C nanosheet at low coverage, i.e., the top of W atom (T), two trigonal sites with superimposing with C (H1), and bottom W atoms (H2). (Supplementary Materials)

References

[1] Z. Fang, L. Peng, H. Lv et al., “Metallic transition metal selenide holey nanosheets for efficient oxygen evolution electrocatalysis,” ACS Nano, vol. 11, no. 9, pp. 9550–9557, 2017.

[2] K. N. Dinh, P. Zheng, Z. Dai et al., “Ultrathin porous NiFeV ternary layer hydroxide nanosheets as a highly efficient bifunctional electrocatalyst for overall water splitting,” Small, vol. 14, no. 8, p. 1703257, 2018.

[3] P. Zheng, Y. Zhang, Z. Dai et al., “Constructing multifunctional heterostructure of Fe2O3@Ni3Se4 nanotubes,” Small, vol. 14, no. 15, p. 1704065, 2018.

[4] Z. Fang, L. Peng, Y. Qian et al., “Dual tuning of Ni-Co-A (A = P, Se, O) nanosheets by anion substitution and holey engineering for efficient hydrogen evolution,” Journal of the American Chemical Society, vol. 140, no. 15, pp. 5241–5247, 2018.

[5] C. Yan, Y. Zhu, Z. Fang et al., “Heterogeneous molten salt design strategy toward coupling cobalt–cobalt oxide and carbon for efficient energy conversion and storage,” Advanced Energy Materials, vol. 8, no. 23, p. 1800762, 2018.

[6] K. N. Dinh, X. Sun, Z. Dai et al., “O2 plasma and cation tuned nickel phosphide nanosheets for highly efficient overall water splitting,” Nano Energy, vol. 54, pp. 82–90, 2018.

[7] I. Gheeley, T. F. Jaramillo, J. Bonde, I. Chorkendorff, and J. K. Nørskov, “Computational high-throughput screening of electrocatalytic materials for hydrogen evolution,” Nature Materials, vol. 5, no. 11, pp. 909–913, 2006.

[8] B. Luo, D. Ye, and L. Wang, “Recent progress on integrated energy conversion and storage systems,” Advanced Science, vol. 4, no. 9, p. 1700104, 2017.

[9] J. Shui, M. Wang, F. Du, and L. Dai, “N-doped carbon nanomaterials are durable catalysts for oxygen reduction reaction in acidic fuel cells,” Science Advances, vol. 1, no. 1, 2015.

[10] Yiluguma, Z. Wang, W. Xu et al., “Bridged-multi-octahedral cobalt oxide nanocrystals with a Co-terminated surface as an oxygen evolution and reduction electrocatalyst,” Journal of Materials Chemistry A, vol. 5, no. 16, pp. 7416–7422, 2017.

[11] H. Yin and Z. Tang, “Ultrathin two-dimensional layered metal hydroxides: An emerging platform for advanced catalysis, energy conversion and storage,” Chemical Society Reviews, vol. 45, no. 18, pp. 4873–4891, 2016.

[12] X. Liu, C. Meng, and Y. Han, “Defective graphene supported MPdI2 (M = Fe, Co, Ni, Cu, Zn, Pd) nanoparticles as potential oxygen reduction electrocatalysts: a first-principles study,” The Journal of Physical Chemistry C, vol. 117, no. 3, pp. 1350–1357, 2013.

[13] K. N. Dinh, Q. Liang, C. Du et al., “Nanostructured metallic transition metal carbides, nitrides, phosphides, and borides for energy storage and conversion,” Nano Today, vol. 25, pp. 99–121, 2019.

[14] E. J. Popczun, J. R. McKone, C. G. Read et al., “Nanostructured nickel phosphide as an electrocatalyst for the hydrogen evolution reaction,” Journal of the American Chemical Society, vol. 135, no. 25, pp. 9267–9270, 2013.

[15] J. Duan, S. Chen, B. A. Chambers, G. G. Andersson, and S. Z. Qiao, “3D WS2 nanolayers/substrate-heteroatom-doped graphene films as hydrogen evolution catalyst electrodes,” Advanced Materials, vol. 27, no. 28, pp. 4234–4241, 2015.

[16] M. Gao, J. Liang, Y. Zheng et al., “An efficient molybdenum disulfide/cobalt diselenide hybrid catalyst for electrochemical hydrogen generation,” Nature Communications, vol. 6, no. 1, p. 5982, 2015.

[17] H. Wang, Z. Lu, D. Kong, J. Sun, T. M. Hykel, and Y. Cui, “Electrochemical tuning of MoS2 nanoparticles on threedimensional substrate for efficient hydrogen evolution,” ACS Nano, vol. 8, no. 5, pp. 4940–4947, 2014.

[18] L. Shang, B. Tong, H. Yu et al., “Hydrogen Evolution: CdS nanoparticle-decorated Cd nanosheets for efficient visible light-driven photocatalytic hydrogen evolution,” Advanced Energy Materials, vol. 6, no. 3, 2016.

[19] J. Zhang, T. Wang, D. Pohl et al., “Interface engineering of MoS2/Ni3S2Heterostructures for highly enhanced electrochemical overall-water-splitting activity,” Angewandte Chemie International Edition, vol. 55, no. 23, pp. 6702–6707, 2016.

[20] M. Cabán-Acevedo, M. L. Stone, J. R. Schmidt et al., “Efficient hydrogen evolution catalysis using ternary pyrite-type cobalt phosphosulfide,” Nature Materials, vol. 14, no. 12, pp. 1245–1251, 2015.

[21] F. Ma, H. B. Wu, B. Y. Xia, C. Xu, and X. W. Lou, “Hierarchical β-Mo2C nanotubes synthesized by ultrathin nanosheets as a highly efficient electrocatalyst for hydrogen production,” Angewandte Chemie, vol. 127, no. 51, pp. 15615–15619, 2015.

[22] X. Fan, H. Zhou, and X. Guo, “WC nanocrystals grown on vertically aligned carbon nanotubes: An efficient and stable electrocatalyst for hydrogen evolution reaction,” ACS Nano, vol. 9, no. 5, pp. 5125–5134, 2015.

[23] S. P. Berglund, H. He, W. D. Chemelewski, H. Celio, A. Dolocan, and C. B. Mullins, “P-Si/W2C and p-Si/W2C/Pt photocathodes for the hydrogen evolution reaction,” Journal of the American Chemical Society, vol. 136, no. 4, pp. 1535–1544, 2014.

[24] D. V. Esposito, S. T. Hunt, A. L. Stottlemeyer et al., “Low-cost hydrogen-evolution catalysts based on monolayer platinum on tungsten monocarbide substrates,” Angewandte Chemie International Edition, vol. 49, no. 51, pp. 9859–9862, 2010.

[25] S. T. Hunt, T. Nimmanwudipong, and Y. Román-Leshkov, “Engineering non-sintered, metal-terminated tungsten carbide nanoparticles for catalysis,” Angewandte Chemie International Edition, vol. 53, no. 20, pp. 5131–5136, 2014.

[26] Q. Luo, T. Wang, G. Walther, M. Beller, and H. Jiao, “Molybdenum carbide catalysed hydrogen production from formic acid - a density functional theory study,” Journal of Power Sources, vol. 246, pp. 548–555, 2014.

[27] R. B. Levy and M. Boudart, “Platinum-like behavior of tungsten carbide in surface catalysis,” Science, vol. 181, no. 4099, pp. 547–549, 1973.
[28] M. C. Weidman, D. V. Esposito, Y.-C. Hsu, and J. G. Chen, “Comparison of electrochemical stability of transition metal carbides (WC, W 2C, Mo 2C) over a wide pH range,” *Journal of Power Sources*, vol. 202, pp. 11–17, 2012.

[29] D. V. Esposito, S. T. Hunt, Y. C. Kimmel, and J. G. Chen, “A new class of electrocatalysts for hydrogen production from water electrolysis: Metal monolayers supported on low-cost transition metal carbides,” *Journal of the American Chemical Society*, vol. 134, no. 6, pp. 3025–3033, 2012.

[30] R. J. Colton, J.-T. J. Huang, and J. W. Rabalais, “Electronic structure of tungsten carbide and its catalytic behavior,” *Chemical Physics Letters*, vol. 34, no. 2, pp. 337–339, 1975.

[31] A. S. Kurlov and A. I. Gusev, “Tungsten carbides and W-C phase diagram,” *Inorganic Materials*, vol. 42, no. 2, pp. 121–127, 2006.

[32] T. Ishii, K. Yamada, N. Osuga, Y. Imashiro, and J.-I. Ozaki, “Single-step synthesis of W2C nanoparticle-dispersed carbon electrocatalysts for hydrogen evolution reactions utilizing phosphate groups on carbon edge sites,” *ACS Omega*, vol. 1, no. 4, pp. 689–695, 2016.

[33] Q. Gong, Y. Wang, Q. Hu et al., “Ultrasmall and phase-pure W2C nanoparticles for efficient electrocatalytic and photoelectrochemical hydrogen evolution,” *Nature Communications*, vol. 7, no. 1, p. 13216, 2016.

[34] H. Ang, H. T. Tan, Z. M. Luo et al., “Hydrophilic nitrogen and sulfur Co-doped molybdenum carbide nanosheets for electrochemical hydrogen evolution,” *Small*, vol. 11, no. 47, pp. 6278–6284, 2015.

[35] D. C. Ghosh and R. Biswas, “Theoretical calculation of absolute radii of atoms and ions. Part 2. The ionic radii,” *International Journal of Molecular Sciences*, vol. 4, no. 6, pp. 379–407, 2003.

[36] K. Xiong, L. Li, L. Zhang et al., “Ni-doped Mo2C nanowires supported on Ni foam as a binder-free electrode for enhancing the hydrogen evolution performance,” *Journal of Materials Chemistry A*, vol. 3, no. 5, pp. 1863–1867, 2015.

[37] X. Fan, Z. Peng, R. Ye, H. Zhou, and X. Guo, “M3C (M: Fe, Co, Ni) nanocrystals encased in graphene nanoribbons: an active and stable bifunctional electrocatalyst for oxygen reduction and hydrogen evolution reactions,” *ACS Nano*, vol. 9, no. 7, pp. 7407–7418, 2015.

[38] C. Wan and B. M. Leonard, “Iron-doped molybdenum carbide catalyst with high activity and stability for the hydrogen evolution reaction,” *Chemistry of Materials*, vol. 27, no. 12, pp. 4281–4288, 2015.

[39] W.-F. Chen, C.-H. Wang, K. Sasaki et al., “Highly active and durable nanostructured molybdenum carbide electrocatalysts for hydrogen production,” *Energy & Environmental Science*, vol. 6, no. 3, pp. 943–951, 2013.

[40] G. Kresse and J. Furthmüller, “Efficiency of ab-initio total energy calculations for metals and semiconductors using a plane-wave basis set,” *Computational Materials Science*, vol. 6, no. 1, pp. 15–50, 1996.

[41] G. Kresse and D. Joubert, "From ultrasoft pseudopotentials to the projector augmented-wave method," *Physical Review B: Condensed Matter and Materials Physics*, vol. 59, no. 3, pp. 1758–1775, 1999.

[42] J. D. Pack and H. J. Monkhorst, "’Special points for Brillouin-zone integrations’—a reply," *Physical Review B: Condensed Matter and Materials Physics*, vol. 16, no. 4, pp. 1748-1749, 1977.