Longitudinal double spin asymmetries in single hadron quasi-real photoproduction at high $p_T$

Abstract

We measured the longitudinal double spin asymmetries $A_{LL}$ for single hadron muoproduction off protons and deuterons at photon virtuality $Q^2 < 1$(GeV/c)$^2$ for transverse hadron momenta $p_T$ in the range 1 GeV/c to 4 GeV/c. They were determined using COMPASS data taken with a polarised muon beam of 160 GeV/c or 200 GeV/c impinging on polarised $^6$LiD or NH$_3$ targets. The experimental asymmetries are compared to next-to-leading order pQCD calculations, and are sensitive to the gluon polarisation $\Delta G$ inside the nucleon in the range of the nucleon momentum fraction carried by gluons $0.05 < x_g < 0.2$.

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1 Introduction

The spin structure of the nucleon is one of the major unresolved issues in hadronic physics. While the quark spin contribution to the nucleon spin, denoted as $\Delta \Sigma$, has been measured to be about 30% [1], the gluon spin contribution is still insufficiently constrained after more than two decades of intense study. In the framework of perturbative Quantum Chromodynamics (pQCD), inclusive Deep Inelastic Scattering (DIS) is sensitive to gluon contributions only through higher-order corrections to the cross section. The spin-averaged gluon density $g(x_g)$, where $x_g$ denotes the nucleon momentum fraction carried by gluons, is well constrained by DIS experiments with unpolarised beam and target because of their high statistics and large kinematic coverage. The fewer data from DIS experiments with polarised beam and target, however, can not sufficiently constrain the gluon helicity distribution $\Delta g(x_g)$. This affects directly our knowledge of the contribution of the gluon spin to the spin of the nucleon, known as $\Delta G = \int \Delta g(x_g) dx_g$, and to a lesser extent that of the quarks [2]. In order to better constrain $\Delta g(x_g)$, one has to resort to processes where contributions from gluons appear at leading order, such as hadron production at high transverse momenta or production of open charm in polarised lepton–nucleon [3, 4, 5, 6, 7] or hadron–hadron interactions [8, 9, 10, 11].

The COMPASS collaboration has already investigated asymmetries of hadrons at high transverse momenta $p_T$, in both the DIS and the quasi-real photoproduction regimes [4, 6, 12]. Here, transverse means transverse with respect to the direction of the virtual photon $\gamma^*$ that is exchanged in the scattering process. Using a Lund Monte Carlo simulation, these measurements were interpreted on the hadron level, thereby simultaneously extracting the gluon helicity on the parton level. Such an analysis is restricted to leading order (LO) in the strong coupling constant $\alpha_s$, as presently there exists no next-to-leading order (NLO) Monte Carlo simulation for leptoproduction. Due to the limitation of neglecting gluon contributions at NLO, such results can not be used in recent global fits at NLO of polarised Parton Distribution Functions (PDFs) [13].

In this Letter, we present a new analysis of COMPASS data for single-inclusive hadron quasi-real photoproduction at high $p_T$ [1], which differs from our previous analysis in that all measured hadrons within a given $p_T$ bin are included in the analysis, and not only the hadron(s) with highest $p_T$. Moreover, the interpretation of the results is based on a collinear pQCD framework that was developed up to NLO [14], the basic concept being the application of the factorisation theorem to calculate the cross section of single-inclusive hadron production. The authors of Ref. [14] discuss the sensitivity of COMPASS data to $\Delta g(x_g)$ in terms of contributions from “direct-photon”, $\gamma^* g \rightarrow q\bar{q}$ (Photon Gluon Fusion), and from “resolved-photon” subprocesses, $qg$ and $gg$, where the photon acts as a source of partons. Similarly, they consider direct $\gamma^* q \rightarrow qg$ (QCD Compton) as well as resolved $qq$ and $gq$ subprocesses for the background. These contributions to the cross section are represented schematically in Fig. [1]. In the framework of collinear fragmentation, photo-absorption on quarks, $\gamma^* q \rightarrow q$, is not contributing to high $p_T$ hadron production.

\footnote{Note that also inclusive quasi-real photoproduction of hadron pairs can be considered [15].}
In order to gain confidence in the applicability of this pQCD framework to single-hadron production with longitudinally polarised beam and target, an important step is to compare predictions of this model to measurements with beam and target unpolarised, for which the PDFs are well known. While good agreement was found by RHIC experiments on the production of high-$p_T$ hadrons in $pp$ collisions at $\sqrt{s} \simeq 200$ GeV [16, 17], complications arise when hard scattering subprocesses are probed in the “threshold” regime, in which large logarithmic contributions from soft and collinear gluons play a significant role [18]. Such contributions become dominant at the COMPASS centre-of-mass energy of $\sqrt{s} \simeq 18$ GeV. When taken into account by a technique known as “threshold resummation” at next-to-leading logarithm (NLL) [18], the calculations reproduce the COMPASS cross section measurements [19] within theoretical uncertainties.

In this Letter, we analyse the quasi-real photoproduction data collected by COMPASS from 2002 to 2011 on longitudinally polarised deuteron and proton targets. In Sec. 2 we give a brief description of the experimental setup, and details on the data selection can be found in Sec. 3. The procedure for the asymmetry determination is described in Sec. 4. In Sec. 5, we present the corresponding double spin asymmetries for single-inclusive hadron production as a function of their transverse momenta $p_T$. These asymmetries are compared to calculations that were performed using the code of Ref. [14], which does not include the resummation of threshold logarithms.

2 Experimental Setup

The measurements were performed with the COMPASS setup using positive muons from the M2 beam line of the CERN SPS. A detailed description of the experimental setup can be found in Ref. [20], with updates valid since 2006 described in Ref. [21]. The muon beam had a nominal momentum of 160 GeV/$c$, except for 2011 where the momentum was 200 GeV/$c$. On average, its momentum spread was 5% and its polarisation was $P_b \approx 0.8$. Momentum and trajectory of incident muons were measured by a set of scintillator hodoscopes, scintillating fibre and silicon microstrip detectors. The beam was scattered off a solid state deuterated lithium ($^6$LiD) target from 2002 to 2006 and off an ammonia (NH$_3$) target in 2007 and 2011, providing longitudinally polarised deuterons and protons, respectively. The target material was placed inside a large aperture superconducting solenoid, and by dynamic nuclear polarisation it was polarised to a value of $P_t \approx 0.5$ for $^6$LiD and $P_t \approx 0.85$ for NH$_3$. Until 2004, the target material was contained in two contiguous 60 cm long cells that were oppositely polarised. From
2006 onwards, three contiguous target cells of length 30 cm, 60 cm and 30 cm were used to minimise systematic effects, with the polarisation in the outer cells being opposite to that in the central one. The direction of the target polarisation was regularly flipped by reversing the solenoid field to compensate for acceptance differences between the different target cells. At least once per year, the direction of the polarisation was reversed relative to that of the solenoid field. The dilution factor \( f \), which accounts for the presence of unpolarisable material, amounts to typically 0.4 for the deuterated lithium target and to 0.16 for the ammonia one. It is calculated as the ratio of the cross section on polarisable deuteron or proton to that on all target nuclei, corrected for unpolarised \( x \) and \( y \) dependent electromagnetic radiative effects [22], where \( x \) is the Bjorken scaling variable and \( y \) the relative muon energy transfer. No further radiative effects are taken into account. The momenta and angles of scattered muons and produced hadrons were measured in the two-stage open forward spectrometer, where each stage includes a dipole magnet with upstream and downstream tracking detectors.

3 Data Selection

In order to be selected, an event must have an interaction vertex that contains both incoming and scattered muons and at least one hadron candidate track. The measured beam momentum is required to be in a \( \pm 20 \) GeV interval around the nominal value (\( \pm 15 \) GeV in 2011). In order to equalise the flux through each target cell, the extrapolated beam track is required to pass all target cells. Cuts on the position of the vertex allow the selection of the target cell, in which the scattering occurred. Only events with photon virtuality \( Q^2 < 1 \) (GeV/c)^2 are accepted. This kinematic region is referred to in the following as quasi-real photoproduction region. In addition, \( y \) is required to be within 0.01 and 0.9, where the lower limit removes events that are difficult to reconstruct and the upper limit removes the region where electromagnetic radiative effects are large. These kinematic cuts result in a range of \( 10^{-5} < x < 0.02 \) and a minimum mass squared of the hadronic final state, \( W^2 \), of 25 (GeV/c^2)^2. The hadron candidate track must have \( p_T > 0.7 \) GeV/c. The fraction \( z \) of the virtual photon energy carried by the hadron is required to be in the range \( 0.2 < z < 0.8 \), where the lower limit is imposed to suppress the contribution from target remnant hadronisation and the upper limit to reject badly reconstructed hadrons. The angle between the direction of the hadron and that of the virtual photon is restricted to be in the range \( 10^{\circ} < \theta < 120^{\circ} \), which corresponds to \( 2.4 > \eta > -0.1 \), where \( \eta \) is the pseudo-rapidity in the \( \gamma^*N \) centre-of-mass system. After all selections, the final sample consists of 140 million events for the deuteron target and 105 million for the proton target.

4 Asymmetry Calculation

The double-spin asymmetry of the cross sections for single hadron quasi-real photoproduction is defined as \( A_{LL} = (\sigma_\uparrow - \sigma_\downarrow)/(\sigma_\uparrow + \sigma_\downarrow) = \Delta \sigma /\sigma \), where the symbols \( \uparrow \) and \( \downarrow \) denote anti-parallel and parallel spin directions, respectively, of the incident muon and the target deuteron or proton. This asymmetry is evaluated using the same method as in our previous analyses [6]. The number of hadrons produced in a target cell is related to \( A_{LL} \) and to the spin independent cross section \( \sigma = \sigma_\uparrow_\gamma + \sigma_\downarrow_\gamma \): \( N_i = \alpha_i \phi_i n_i(1 + f_i P_o P_i A_{LL}) \), where \( i = u_1, d_1, u_2, d_2 \). A target cell \( (u \) or \( d \)) with a given direction of the target polarisation \( (1 \) or \( 2 \)) has the acceptance \( a_i \), the incoming muon flux \( \phi_i \) and the number of target nucleons \( n_i \). For the two-cell target, \( u \) and \( d \) denotes upstream and downstream cell, respectively, while for the three-cell target, \( u \) denotes the sum of the outer cells and \( d \) the central cell. The asymmetry \( A_{LL} \) is extracted from the second order equation that is obtained from the quantity \( (N_{u_1} - N_{d_1})/(N_{u_1} + N_{d_1}) \). In this relation, fluxes and acceptances cancel, provided that the ratio of acceptances of the two sets of cells is equal for the two orientations of the solenoid field.

In order to minimise statistical uncertainties, all quantities entering the asymmetry are calculated for each hadron using a weight factor \( w_i = f_i P_o \) [23]. The muon beam polarisation \( P_o \) is obtained from a
parametrisation as a function of the beam momentum. The target polarisation $P_t$ is not included in the weight $w_i$ as it changes with time and could generate false asymmetries. In order to reduce systematic uncertainties, data are grouped into periods that are close in time and hence have the same detector conditions, and the weighted average over all periods is taken. The asymmetries determined for a given target from data taken in different years were found to be consistent and hence combined. The asymmetries are obtained for both positive and negative unidentified hadrons in bins of $p_T$ in the range 0.7 GeV/c to 4 GeV/c and in bins of $\eta$ in the range $-0.1$ to 2.4 in order to facilitate a detailed comparison to theory (see Sec. 3). The data for $p_T < 1.0$ GeV/c are only used to investigate systematic uncertainties as the pQCD framework is commonly applied only for hard scales $\mu^2 \approx p_T^2 \gtrsim 1.0$ (GeV/c)$^2$, and they are shown greyed out in all the figures where they appear in.

The systematic uncertainties on $A_{LL}$ are calculated as the square root of the sum of squares of multiplicative and additive contributions. The uncertainties on the dilution factor ($\approx 5\%$), the beam ($\approx 5\%$) and the target ($\approx 5\%$) polarisations contribute to a total of $\approx 8\%$ of multiplicative uncertainties, i.e. those being proportional to the asymmetry itself. Additive contributions originate from fluctuations of the detector performance, which may lead to false asymmetries. Their possible occurrence is investigated by dividing the data sample into different subsets. Asymmetries calculated with hadrons detected in left and right (top and bottom) parts of the spectrometers are found to be compatible within statistical uncertainties, as well as those for the two relative orientations of the solenoid field and the target spin vectors. No systematic uncertainty is thus attributed to these effects. Possible false asymmetries between data sets having the same polarisation states are also found to be compatible with zero. For each $p_T$ bin, the statistical distribution of the asymmetries calculated by time periods closely follows a normal distribution. The observed deviations from a Gaussian allow us to quantify the level of overall additive systematic uncertainties as a fraction of the statistical ones, which on average amounts to about one half. These additive systematic uncertainties largely dominate over the multiplicative ones.

5 Results and interpretation

The final asymmetries are calculated using all data accumulated with the deuteron target in the years 2002 to 2006 and with the proton target in the years 2007 and 2011. Their $p_T$-dependence in three rapidity bins spanning the full interval $-0.1 < \eta < 2.4$ ($[-0.1, 0.45]$, [0.45, 0.9], and [0.9, 2.4]) is shown in Fig. 2 and Fig. 3 for each target type and hadron charge.

We compare our asymmetries with theoretical calculations at NLO without threshold resummation based on the framework described in Ref. 14 and summarised in the following. Using the code of Ref. 14, the asymmetries are computed in bins of $p_T$ and $\eta$ as the ratio of polarised to unpolarised hadron cross sections, where a cross section is a convolution of the "muon–parton distribution function" $f^\mu_a$, the nucleon PDFs $f_b^N$, the perturbative partonic cross sections $\hat{A}_{a+b\rightarrow c+X}$, and the fragmentation functions (FF) $D_b^c$:

$$A_{LL}(p_T, \eta) = \frac{d\sigma^h}{d\sigma^T}(p_T, \eta) = \sum_{a,b,c} \frac{\Delta f^\mu_a \otimes \Delta f^N_b \otimes d\Delta \hat{A}_{a+b\rightarrow c+X} \otimes D_b^c}{\sum_{a,b,c} f^\mu_a \otimes f_b^N \otimes d\Delta \hat{A}_{a+b\rightarrow c+X} \otimes D_b^c}.$$  \hspace{1cm} (1)

Here and below, spin-dependent quantities are denoted by the symbol $\Delta$ and will be referred to as polarised ones in the rest of the Letter (spin-independent ones as unpolarised). The processes involved in Eq. 1 can be classified into "direct" ones that are initiated by a quasi-real photon and "resolved" ones that are initiated by its fluctuation into partons. This classification is denoted by the subscript $a$ (see Fig. 1). For direct processes, subscript $a$ refers to $\gamma^*$, and $\langle \Delta f^\mu_a \rangle$ is the probability for a muon to emit a quasi-real photon. For resolved processes, subscript $a$ refers to $q$, $\bar{q}$ or $g$, and $\langle \Delta f^\mu_a \rangle$ is the convolution of this probability with a non-perturbative parton distribution of the photon, $\langle \Delta f^\gamma_a \rangle$. The polarised version
Fig. 2: The asymmetry $A_{LL}$ as a function of $p_T$ for charged hadron quasi-real photoproduction on the proton for three rapidity bins. The bands at the bottom indicate the systematic uncertainties, which are dominated by time dependent fluctuations (see Sec. 4.) Top: positive hadron production; bottom: negative hadron production.

Fig. 3: Same as Fig. 2 but for the deuteron.
of the latter is not known experimentally and hence taken to range between the positive and negative magnitude of the unpolarised one. This induces a small uncertainty in the theoretical calculations.

The values of the asymmetries are computed here using the following input distributions: the unpolarised parton distributions of the photon $f_1^\gamma$ from GRSL [24], the unpolarised nucleon PDFs $f_1^n$ from CTEQ65 [25], the three polarised PDF sets from GRSV [26] as in Ref. [14] (the “standard” set and the two sets for “maximum” $[\Delta g(x) = g(x)]$ and “minimum” $[\Delta g(x) = -g(x)]$ gluon distribution functions at input scale), as well as the most recent polarised PDF set DSSV14 from Ref. [13]. For the polarised PDF sets used, the integration over the range $0 < x < 2$, which is characteristic for the kinematic coverage of COMPASS in the gluon momentum fraction, yields the following “truncated” values of $\Delta G$ at a scale of 3 (GeV/c)$^2$: $\Delta G_{GRSV_{\text{max}}} \approx -0.6$, $\Delta G_{DSSV_{14}} \approx 0.1$, $\Delta G_{GRSV_{\text{min}}} \approx 0.2$, $\Delta G_{GRSV_{\text{max}}} \approx 0.7$. The other inputs that we changed with respect to Ref. [14] are the fragmentation functions $D_h^p$, for which we use the most recent parton-to-pion fragmentation set of Ref. [27], which best fits the recent COMPASS pion multiplicities [28]. We checked, as it was done in Ref. [14], that asymmetries for hadron and pion production are almost indistinguishable, so that it is safe to compare our experimental data to theoretical asymmetries computed with a parton-to-pion FF set. The fractions of the total unpolarised (respectively polarised) cross section for the various individual subprocesses are shown in Fig. 4 as a function of $p_T$. Although the unpolarised cross sections for processes involving gluons from the nucleon are not the dominant ones, the polarised cross section for the $\gamma g$ subprocess is large in magnitude for hadron production at high $p_T$, which makes the study of such asymmetries relevant in the COMPASS kinematic region.

![Fig. 4: Contributions of the six subprocesses $a + b \rightarrow c + X$ described in Sec. 1 to the full NLO unpolarised (left) and polarised (right) photoproduction cross sections for a deuteron target. The polarised cross sections are computed using the polarised PDF set of Ref. [13].](image)

The computations of $A_{LL}(p_T)$ are performed at COMPASS kinematics using the same cuts as in the present data analysis, i.e., $p_T > 1$ GeV/c, $Q^2 < 1$ (GeV/c)$^2$, $0.1 < y < 0.9$, $0.2 < z < 0.8$. For consistency, we verified that when using the same inputs as in Ref. [14], we reproduce the asymmetry calculated there. The computations are done separately for the production of positive and negative hadrons, and for three distinct bins in $\eta$: $[-0.1, 0.45]$, $[0.45, 0.9]$, and $[0.9, 2.4]$. The results of these computations are compared to the experimental asymmetries in Fig. 5 and Fig. 6.

The data are seen to be consistent with the NLO calculations of Ref. [14], using the most recent polarised PDF [13] and FF [27] sets, except for positive hadron production from the proton in the rapidity range $-0.1 < \eta < 0.9$. Our data are also compared in Fig. 5 and Fig. 6 to calculations using earlier GRSV polarised PDFs [26] to give an impression of their sensitivity to $\Delta G$, which seems enhanced at higher values of $\eta$. A possible reason for the discrepancy seen at low $\eta$ in positive hadron production from the proton may be that the model calculations had to be done without threshold resummation at NLL, as the formalism for the polarised case is not yet fully available. However, contrary to the unpolarised case
Fig. 5: COMPASS asymmetries $A_{LL}$ for a proton target as a function of $p_T$ and in three rapidity bins, compared to NLO calculations based on Ref. [14] for different choices for the polarised PDFs (see text). Only statistical uncertainties are shown. Error bands on the theory curves represent the uncertainties due to the polarised parton distribution of the photon. Top: positive hadron production; bottom: negative hadron production.

Fig. 6: Same as Fig. 5 but for a deuteron target.
where data can only be described by pQCD if threshold resummation is included \cite{18}. Spin asymmetries are expected to be less affected \cite{29}. A first estimation of the impact of threshold resummation on our double spin asymmetries including so far only the direct processes \cite{30} indicates a substantial dilution of the asymmetries, which may explain part of the discrepancy between experiment and theory for positive hadron production on the proton at low values of $\eta$.

6 Summary

In summary, we have presented in this Letter a new analysis of COMPASS data on polarised single-inclusive hadron quasi-real photoproduction, which in principle is well suited for an extraction of the gluon polarisation $\Delta G$ in the framework of collinear pQCD. Results for the longitudinal spin asymmetry $A_{LL}(p_T)$ on polarised protons and deuterons are given separately for positively and negatively charged hadrons, and in three rapidity bins. They are compared to theoretical calculations at NLO without threshold resummation and overall agreement is found with the calculations based on earlier GRSV$_{std}$ and recent DSSV14 polarised PDF sets, and using the most recent FF set. Nevertheless, calculations including full threshold resummation at NLL are needed before a meaningful result on $\Delta G$ can be extracted quantitatively from our data.

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