Protein-mediated looping of DNA under tension requires supercoiling

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ABSTRACT

Protein-mediated DNA looping is ubiquitous in chromatin organization and gene regulation, but to what extent supercoiling or nucleoid associated proteins promote looping is poorly understood. Using the lac repressor (LacI), a paradigmatic loop-mediating protein, we measured LacI-induced looping as a function of either supercoiling or the concentration of the HU protein, an abundant nucleoid protein in Escherichia coli. Negative supercoiling to physiological levels with magnetic tweezers easily drove the looping probability from 0 to 100% in single DNA molecules under slight tension that likely exists in vivo. In contrast, even saturating (micromolar) concentrations of HU could not raise the looping probability above 30% in similarly stretched DNA or 80% in DNA without tension. Negative supercoiling is required to induce significant looping of DNA under any appreciable tension.

INTRODUCTION

Protein-mediated DNA looping is a ubiquitous feature of gene regulation and other DNA transactions (1–4). The paradigmatic lac repressor (LacI)-mediated loop inhibits the expression of the lac operon in Escherichia coli (5), and the looping probability is set by LacI tetramer concentration, binding site affinities, and the loop size (6,7). Indeed, loops secured by a single LacI tetramer bridging two binding sites (operators) are suppressed when separate LacI tetramers occupy both operators, or when either the stiffness of short, or entropy of long, intervening DNA overwhelms the free energy of protein binding (8,9). Thus, ~500 bp-long DNA segments most easily form LacI-mediated loops (9) at intermediate LacI concentrations (7,10).

In vivo, bacterial DNA is extensively decorated and configured by nucleoid associated proteins (NAPs), including the abundant histone-like U (HU) protein (11), which compacts DNA into a flexible HU-DNA filament in 150–200 mM salt (12). HU potently changes the bacterial transcriptome (11), and binding correlates with negative supercoiling in stationary phase E. coli (13). 500 nM or more HU also drives LacI-mediated looping of ~140 bp DNA to maxima without altering the binding of LacI (14).

Supercoiling has been also shown to dynamically coordinate the transcription of bacterial (15,16) as well as eukaryotic genes (17,18), and the overall level of supercoiling is an indicator of cell health (19,20). Supercoiling is widely and inhomogeneously distributed in the bacterial chromosome, being generated by the binding of nucleoid-associated proteins, such as HU (21,22), and by various DNA transactions (13,23). Negative supercoiling stabilizes regulatory DNA loops, for example, those that repress the lytic genes of bacteriophage λ (24,25) or the gal or lac operons (26,27). Such loops act as barriers to supercoiling diffusion and confine supercoiling density (25,28) as part of biochemical interplay in which supercoiling promotes looping and loops constrain stabilizing superhelical density.

Small and large loops have different energy barriers to formation, but supercoiling and nucleoid-associated proteins may enhance looping in both cases. They can be distinguished by comparing the loop segment to the persistence length of DNA, ~150 bp (~50 nm). For small loops on the order of a persistence length or less, energy is required to kink or bend the short, stiff segment of DNA and juxtapose DNA segments for looping, as well as to twist the intervening DNA segment to orient both DNA binding sites toward the protein that joins them. Supercoiling can modify the twist of DNA to minimize the difference in rotational orientations of two binding sites about the helical axis (29). In this way a small, bidentate protein can simultaneously bind two sites on the same face of the helix to produce a loop. Several reports in the literature have shown that the probability of forming loops oscillates as a function of the rotational offset determined by the contour length between the binding sites (30–32). This may be important for loops between the O1 and O3 operators of the lac operon in E. coli, which are separated by a torsionally rigid 92 bp segment, and may be relevant to observations of the supercoiling-driven modulation of in vivo repression of a reporter gene.
by protein-mediated DNA loops 70–85 bp-long (33). As shown previously, supercoiling-induced and HU-stabilized kinks likely bent the segment and optimized the orientation of the binding sites enhanced the formation of the 113 bp loop mediated by the gal repressor (27). Thus, there is clear evidence that HU and supercoiling may enhance the formation of short loops, whether or not the mechanism involves plectonemes.

For long, flexible loops, the foremost barrier is the separation between the binding sites (34). This is especially critical in DNA under tension which extends the molecule and favors twist over writhe, which opposes juxtaposition of the protein binding sites for looping. Proteins like RNA polymerase intermittently translocate DNA, creating as much as 20 pN of tension before stalling (35). This intermittent activity will modulate the twist/writhe equilibrium and thereby the opportunity for proteins like the lac repressor to secure loops. As will be shown below, supercoiling-induced plectonemes draw binding sites together to promote looping. The O2 and O1 operators of the lac operon in E. coli are separated by a 401 bp. The intrinsic flexibility of such a long span relieves flexural and torsional strain and randomizes the orientations of juxtaposed binding sites. Nevertheless, in vitro experiments from thirty years ago on similarly long segments showed that supercoiling enhanced looping (36). Those experiments which did not include protein factors, like HU, that might modify looping in vivo, did not lead to a mechanical view of how supercoiling enhances the looping of long segments and whether accessory proteins can produce similar effects.

More recently, in vivo levels of LacI-mediated looping were found to be higher than those measured in vitro for a range of large loop sizes in identical DNA templates (7). To determine whether NAPs and/or supercoiling were likely to have caused the differences, the probabilities of LacI-mediated DNA loops in single DNA molecules have been measured as a function of either the superhelicity of the tether, or the concentration of HU for DNA molecules under little or no tension. Both parameters progressively decreased the fractional extension of DNA under 0.25 pN of tension and enhanced looping, but only supercoiling drove the formation of stable loops in DNA under higher tension.

**MATERIALS AND METHODS**

**Preparation of DNA constructs**

All DNA fragments for TPM experiments were amplicons of PCR reactions with plasmid DNA pYY11400_BstEI (37) or pO1O2 (26) as templates with dNTPs (Fermentas-Thermo Fisher Scientific Inc., Pittsburgh, PA, USA), digoxigenin- and biotin-labeled primers (Integrated DNA Technologies, Coralville, IA, or Invitrogen, Life Technologies, Grand Island, NY, USA) (Supplementary Table S1) and Taq Polymerase (New England BioLabs, Ipswich, MA, USA). The total lengths of the DNA constructs Os-400-O1 and O1-400-O2 were 909, and 831 bp respectively with centrally located, 400 bp, LacI-inducible loops as diagrammed in Supplementary Figure S1.

DNA tethers for magnetic-tweezers experiments were generated by ligating a 2115 bp main construct containing the O1-400-O2 sequence with a centrally positioned, 400 bp, LacI-inducible loop (Supplementary Figure S1), to ~1 kb digoxigenin- and biotin-labeled DNA fragments at opposite ends with T4 DNA ligase (New England Biolabs, Ipswich, MA, USA). This procedure has been used previously to produce similar, torsionally restrained DNA tethers (38). The main construct was a PCR amplicon produced with an equimolar dNTP mix and primers including ApaI or XmaI restriction digest sites. The ~1 kb biotin-or digoxigenin-labeled DNA fragments for anchorage were generated by ApaI or XmaI restriction digestions of ~2 kb PCR amplicons produced using dATP, dCTP, dGTP, dUTP (Fermentas-Thermo Fisher Scientific Inc., Pittsburgh, PA, USA) and digoxigenin-11-dUTP (Roche Life Science, Indianapolis, IN, USA) or biotin-11-dUTP (Invitrogen, Life Technologies, Grand Island, NY, USA) in a molar ratio of 1:1:1:0.9:0.1. After digestion and purification with silica-membrane-based kits (Qiagen, Germantown, MD, USA), the main and the anchorage fragments were ligated with T4 ligase. Random, 10% incorporation of the biotin- and digoxigenin-dUTP labels in the sequences bordering the ApaI and XmaI restriction sites in the pBlueScript KS(+) template used here, will place the first label from 6 to 71 bp away from the ligation junctions to the anchorage fragments in 95% of the molecules (Supplementary Figure S2). Therefore, the total length variation in the DNA tether due to labeling will not exceed 14–127 bp (38 nm). Multiple labels along the anchorage segments is necessary to torsionally restrain the DNA tethers.

**Microchamber preparation**

Microchambers were prepared similarly to what has been previously described (25,39). In brief, a microchamber with ~30 µl volume was created between two glass coverslips (Fisherbrand, Thermo Fisher Scientific, Waltham, MA, USA) separated by a parafilm gasket with a narrow inlet and outlet to reduce evaporation of the reaction buffer, and a wide, central observation area (40). DNA tethers were attached through a digoxigenin at one end to the chamber bottom passivated with anti-digoxigenin (Roche Life Science, Indianapolis, IN, USA) and at the other end to either a 320-nm-diameter streptavidin-coated polystyrene bead (Spherotech, Lake Forest, IL, USA) for TPM experiments or a 1.0-µm-diameter streptavidin-coated paramagnetic bead (Dynabead MyOne Streptavidin T1, Invitrogen, Life Technologies, Grand Island, NY, USA) for magnetic tweezing. The chamber was filled with a 10 mM Tris–HCl (pH 7.4), 200 mM KCl, 0.5 mg/ml α-casein buffer and stored in a sealed box to maintain high humidity at 4°C. Before use the chamber was flushed with 200 µl of λ buffer (10 mM Tris–HCl (pH 7.4), 200 mM KCl, 5% DMSO, 0.1 mM EDTA, and 0.1 mg/ml α-casein).

**Tethered particle motion (TPM) experiments**

All LacI and HU titration TPM experiments were conducted in λ buffer at room temperature. For HU titration experiments, the concentrations of LacI were fixed at 5 or 2.5 mM for Os-400-O1 and O1-400-O2 DNA respectively, to give ~25% looping probabilities without HU (Supplementary Figure S3).
Magnetic tweezer experiments

A magnetic tweezer (MT) was used to supercoil DNA and to assay the dynamics of LacI-mediated loop formation. The MT consists of permanent magnets that can be translated along and rotated about the optical axis of the microscope to vary the strength of a laterally oriented magnetic field in the microchamber (44,45). Single DNA tethers were identified through extension vs. twist measurements. Under a high tension of 2 pN, overwound DNA adopts a pleotactic form that smoothly reduces the DNA extension. In contrast, nicked DNA swivels about single bonds to relax any micromotion that smoothly reduces the DNA extension. In contrast, nicked DNA swivels about single bonds to relax any twist setting, would have a measurable effect. Stretching DNA tethers under high tension (sion does not decrease. Stretching DNA tethers under high tension in each condition before adding LacI protein. After adding 1 nM LacI protein, x, y, z and t data were recorded for 20 min at selected tension and twist settings. The DNA extension versus time data were then analyzed to identify probable looping events. A custom MatLab ‘change point’ algorithm followed by an expectation-maximization routine (46,47) was applied to determine the duration of looped (τL) and unlooped (τU) states, and the looping probability was calculated as: \( \sum \tau_L / (\sum \tau_L + \sum \tau_U) \). The free energy change was calculated using \( \Delta G/kT = -\ln(\tau_L/\tau_U) \).

Estimation of the HU concentration in an E. coli cell

Escherichia coli is a rod-shaped bacterium measuring ~1 μm in diameter and 2 μm in length. The volume of a cylindrical E. coli cell is therefore

\[
V = \pi r^2 L = 3.14 \times \left( 0.5 \times 10^{-6} \right)^2 \times \left( 2 \times 10^{-6} \right) \text{ m}^3
\]

\[
= 1.57 \times 10^{-18} \text{ m}^3 = 1.57 \times 10^{-15} \text{ L}
\]

The number of HU proteins in an E. coli cell (in logarithmic phase) has been estimated to range between 30 000 and 55 000 copies (48,49). The number of moles of HU protein in an E. coli cell with 50 ~10^4 copies equals

\[
5 \times 10^4 \text{molecules/6.02} \times 10^{23} \text{molecules} \cdot \text{mol}^{-1}
\]

\[
= 8.3 \times 10^{-20} \text{mol}
\]

and the concentration of HU protein = \( \frac{8.3 \times 10^{-20} \text{mol}}{1.57 \times 10^{-15} \text{L}} = 5.29 \times 10^{-5} \text{M} \). Thus, the concentration range of HU protein is ~30–60 μM.

RESULTS

Looping probability depends on operator affinity

In tethered particle microscopy (TPM), the amplitude of the Brownian motion of a bead tethered by a single DNA molecule to the glass surface of a microscope flow-chamber is monitored over time. A typical experimental recording from TPM assays for two different constructs, Os-400-O1 and O1-400-O2 (Supplementary Figure S1) exhibited intermittent switching of the excursions of beads between one high and two low levels (Figure 1A), as reported for previous measurements of LacI-mediated looping (Figure 1B) (7,50,51). Multiple recordings from each condition were analyzed as described in the methods to determine the fractions of time spent in the looped and unlooped states.

At a LacI concentration of 0.1 nM, the looping probability in Os-400–O1 tethers reached a maximum of almost 90% versus only 45% for O1-400-O2 tethers (Supplementary Figure S3), indicating that the operator affinity affected the maximum looping probability as observed previously for smaller loops (32). Higher concentrations of LacI decrease the looping probability as both of the operator sites become occupied by separate LacI tetramers. We chose concentrations that produced 25% looping probabilities, so that changes in looping by increased HU concentration, or supercoiling, would have a measurable effect.
**Figure 1.** Experimental schematics and representative data. (A) A representative recording of mean squared excursion versus time shows intermittent changes in the average excursion of the bead as LacI-induced looping changes the overall tether length in a 909 bp Os-400-O1 DNA tether. At right, a histogram of the excursion values for the recordings exhibits three peaks which represent the two looped states and the unlooped state fitted with Gaussian curves, shown in red, yellow, and purple respectively. Similar data were recorded for 831-bp-long O1-400-O2 tethers (not shown). (B) A schematic representation of tether length changes due to LacI-induced DNA looping during a TPM experiment (not to scale). (C) A schematic representation of writhe created using a magnetic tweezer and trapped within a LacI-mediated loop (not to scale). Red/green dots indicate biotin/streptavidin linkages of DNA to beads. Orange diamonds/blue crosses indicate digoxigenin/antidigoxigenin linkages of DNA to glass. O1-400-O2 DNA looped by LacI is shown to trap three negative (-) supercoils. The north and south poles of magnets above the microscope stage create a magnetic field to attract and rotate the bead to allow stretching and twisting of the DNA. (D) Recordings of the extension of a 2115 bp-long O1–400-O2 DNA tether under 0.45 pN of tension at different levels of negative supercoiling in the absence (blue) and in the presence (black) of LacI. Extended (unlooped) states dominate at low negative linking number values but become intermittent and finally disappear altogether as negative supercoiling increases and favors the looped state.

**HU decreased tether lengths and promoted LacI-mediated looping**

After establishing a concentration of LacI to set a baseline level of looping, increasing amounts of the HU protein were added to determine the effect on looping. In previously published magnetic tweezer experiments, the salt concentration affected the binding of HU to DNA (12). At monovalent salt concentrations in the range between 150 and 200 mM, increasing the HU concentration produced compaction and increased the flexibility of extremely long, 48 kbp, DNA tethers (12). At least 500 nM, HU also contracted 445 bp DNA tethers by 7% and drove LacI-mediated looping of short, roughly 140 bp, DNA segments to maximum levels without altering the binding of LacI (14). To test whether or not HU similarly affects looping of DNA segments longer than a persistence length, the looping probability was measured as HU protein was titrated from 0 to ~1 μM, a high concentration yet still below maximum estimates for exponentially proliferating *E. coli* (~50 μM, see materials and methods; (48)). For Os-400-O1 or O1-400-O2 tethers in the presence of LacI, excursions of beads, $<\rho^2>$, tethered by both the looped and unlooped DNA decreased as the HU concentration increased (Figure 2A, Supplementary Figure S4). To establish the associated looping probabilities, combinations of three Gaussian curves were fit to histograms of the excursion values aggregated from recordings in identical conditions (Supplementary Figure S4). As [HU] increased, the DNA tethers contracted to reduce excursions of the
attached beads. The fractional extension of the unlooped tether contracted more than the looped tethers (Supplementary Figure S5). Since HU should bind randomly along the tether, this is most likely due to the greater contraction of centrally located, HU-induced bends compared to those in the flanking ends. This effect has been used previously in circular permutation assays to discover the location and extent of protein-induced bends in DNA segments (52).

The looping probability was calculated as the area of all the Gaussian distributions for the looped states divided by the area of the combination of three Gaussians representing all the states. As HU gradually contracted the DNA tether and decreased excitations, the looping probability increased from 25 to a plateau near 80% (Figure 2A). Apparent contour lengths of the DNA tethers were determined from measurements of mean square extensions of beads (Supplementary Table S3), which in λ buffer are related to the contour length of the DNA tether by: \( \langle \rho^2 \rangle = 100.89 \times L + 3445 \) (42).

The fractional extension of the DNA dropped by 50%.

Supercoiling can also contract DNA when the torsional strain exceeds the buckling threshold and the molecule forms plectonemes. Supercoiling was recently shown to enhance λ repressor (CI)-mediated looping in both linear and circular DNA (24, 25). It influences gene expression (53, 54) and is a ubiquitous feature of genomes. To quantitatively characterize the impact of supercoiling on LacI-mediated looping, the probability of the looped state was characterized while gently stretching and twisting 2115 bp DNA tethers using a magnetic tweezer (see schematic in Figure 1C). Experiments on tethers with a centrally located O1-400-O2 loop sequence (Supplementary Figure S1) were carried out at 0.25, 0.45 and 0.75 pN, in the presence of 1 nM LacI. No looping occurred without LacI (Figure 1D, black recordings) or with LacI acting on torsionally relaxed tethers under tension (Figure 3A), because such tension precludes juxtaposition of operators separated by 400 bp, ~130 nm, along the tether (55, 56). However, superhelical densities between −1.9 and −3.4% induced switching between looped and unlooped states (Figure 1D, black recordings). Under low tension, DNA tethers buckle randomly to form plectonemes that rapidly slither or hop to different locations along the length out HU, \( L_f = L_{HU}/L_0 \). Figure 2B shows that HU shifted the looped/unlooped equilibrium to 80% looped when the fractional extension of the DNA dropped by 50%.

Applying tension opposed the HU-driven contraction restoring the extended state and reducing the looping probability. At 1 μM HU concentration, which produced 80% looping in DNA without tension, 0.25, 0.45 or 0.75 pN of tension reduced the probability of looping to 30, 5 or 0% (Figure 2B). Although the contraction that was induced by HU (Figure 2B, green arrow) was essentially reversed by tension (Figure 2B, red arrow), for a given extension, the percentage of looping depended on the concentration of HU and the tension. Thus, the induction of looping by HU can be reversed with tension and appears to be related to the contraction of DNA. A reduction of the overall extension of the DNA does not indicate that the DNA is shorter, because the contour length is unchanged. It indicates random coiling. We have compared the extension of rotationally unconstrained DNA to the looping probability, because coiling creates juxtaposed binding sites that can be linked by the lac repressor to form loops. The HU protein stabilizes large bends in DNA and may induce coiling in rotationally free DNA tethers like those in the TPM experiments described in the manuscript. However, even slight tension opposes coiling and reverses the enhancement of looping by HU. The looping probability drops sharply with slight tension, so that a DNA tether that is partially saturated with HU exhibits a much higher probability of looping without tension than a similarly extended, HU-saturated DNA tether under 0.25 pN of tension. The difference is that HU binding induces kinks in a DNA tether under no tension that reduce the overall extension by 45% and promote random coiling. Slight tension extends the kinked tether which reduces the frequency of juxtaposition of binding sites required for lac repressor to secure a loop.

Supercoiling decreased tether lengths and induced LacI-mediated looping

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Supercoil-driven, LacI-mediated looping exhibited several noteworthy features. First, at each tension, looping probability increased from 0 to 100% as superhelical density became more negative (Figure 3A). The superhelical density of the tethers is \( \sigma = (L_k - L_{k0})/L_{k0} = n/L_{k0} \), where \( L_k \) and \( L_{k0} \) are the linking numbers of twisted and relaxed DNA respectively, and \( n \) is the number of mechanically introduced twists. \( L_{k0} \) is given by the total length in base pairs divided by 10.4 bp per turn. Additional superhelicity lowered the free energy, \( \Delta G \), for looping at each tension (Supplementary Figure S6) and negative superhelicity was more effective than positive. Second, the free energy change for LacI-induced looping as a function of supercoiling was compared with data for the formation of a 393 bp DNA loop by the A repressor protein (CI) (25), which secures looping via cooperative interactions amongst multiple dimers. Negative supercoiling decreased the free energy for LacI- more than for CI-mediated looping (Supplementary Figure S6). These free energy measurements support theoretical investigations indicating that the free energy change for 400 bp LacI-mediated looping in vivo is \(-10 \text{kcal/mol} (-4.4 \text{ kT})\) or less (61).

Third, overlay of the looping probability versus twist measurements with the DNA extension versus twist curves (Figure 3A), revealed that the onset of loop formation induced by negative supercoiling coincided with the onset of plectoneme formation. Indeed, in DNA tethers under tension, plectoneme formation was essential for looping, and more extreme (negative) supercoiling densities were required at higher tensions to achieve similar looping probabilities.

The coincidence of the initial increase in looping probability and plectoneme formation suggested that contraction juxtaposes binding sites for LacI looping. Graphically comparing the contraction of a DNA tether and the associated LacI-mediated looping probability shows that the percentage of looping resembles the percentage of contractions below a threshold that is one loop length shorter than the full-length, unlooped tether, such as that produced when LacI secures a loop. After introducing -2% negative supercoiling during an extension-vs.-twist experiment at 0.45 pN, momentary tether lengths (Supplementary Figure S7 grey points) occasionally dip below a level that is one loop segment shorter (Supplementary Figure S7 red dashed line) and the looping probability begins to rise. With additional negative supercoiling, more measurements fall below that level and the looping probability increases, finally reaching 100%. This is also reflected in extension versus time records which display increases in the frequency and duration of intermittent looping as a DNA tether is negatively supercoiled (Figure 1D), until the looped state becomes perpetual.

If contraction of the DNA were indeed the mechanism by which supercoiling induced looping, then it would be expected to dictate the looping probability independently of the tension. To quantitatively examine this relationship, the fractional extension was defined as the tether extension at a given supercoiling density divided by that of torsionally relaxed DNA, \( L_e = L_0/\sigma \). In Figure 3B, plots of the looping probability associated with different levels of negative supercoiling at three levels of tensions are shown. The looping probability began to rise after supercoiling induced contraction to 0.9–0.95 of the torsionally relaxed extension. Thereafter, the looping probability rapidly increased, and tethers...
DISCUSSION AND CONCLUSION

Contraction, especially with writhe, enhances loop formation

The conformation of DNA stretched and twisted to the buckling point under different tensions rapidly fluctuates between plectonemic and extended conformations (60). Comparison of the onset of loop formation in Os-400-O1 DNA constructs under different tensions (Figure 3B), shows that LacI-mediated loops begin to form just beyond the buckling threshold at which plectonemes form. The contraction of DNA caused by the initial plectonemic gyre has been studied as a function of tension using an optical tweezer with high temporal resolution. This gyre of DNA is about 130 nm-long under 0.45 pN of tension (60). The LacI-induced loop is similarly sized, and this coincidence indicates that lac repressor captures and stabilizes loopsed configurations produced by writhe. Indeed, Supplementary Figure S7 shows that the looping probability correlates with the probability that a tether exhibits an instantaneous extension with at least one loop length of slack. This is the only way in which LacI, which is not a DNA translocase, can establish DNA loops.

HU also seems to promote looping by reducing the fractional extension. It is noteworthy that saturating HU promoted looping more effectively in DNA tethers without tension. Although equivalent levels of contraction were produced in tethers exposed to various concentrations of HU without tension and other tethers exposed to saturating levels of HU and varying levels of tension, the looping probabilities observed for tethers under tension were much lower (Figure 2B). This is likely due to the fact that tension opposes juxtaposition of the protein binding sites and looping even in a DNA tether with a saturating level of HU-induced kinks.

Tension is likely to be physiologically relevant for at least three reasons: First, models for the hierarchical packaging of DNA into chromatin include loops ranging from 15 kb segments in Caulobacter crescentus (62) to hundreds of kbps in mammals (63), and supercoiling appears to be critical for these models. The Meiners laboratory has shown that sub-piconewton tensions can prevent the formation of 305 bp loops (34), and even femtonewton-scale tensions would significantly interfere with loop formation in much larger segments and interfere with hierarchical packaging. Indeed, novobiocin treatment of Caulobacter crescentus cells, which inhibits DNA gyrase and lessens negative supercoiling, altered interactions between segments separated by 20–800 kbp (62). Our finding that supercoiling rescues loop formation in DNA under tension, suggests that DNA in vivo is under tension and that supercoiling is required to condense chromatin through plectoneme formation and looping. Second, in vitro experiments have shown that the translocation velocity of RNA polymerase is unaffected by up to 20 pN of opposing tension on the DNA (35), and that the nucleic acid translocation enzyme that packages DNA into the p29 bacteriophage exerts as much as 50 pN of tension on the DNA (64). It is unlikely that these enzymes would have evolved such capabilities unless they operate against mechanical tension. Third, the Belmont and Wang labs have recently demonstrated that the tension exerted by forces applied to microscopic beads attached to the surface of a cell can be transmitted to the nucleus where it draws segments of chromatin apart and simultaneously enhances transcription from genes in the intervening DNA (65). This demonstration of enhanced transcription by stretching chromatin in a live cell suggests that cells in mechanically distorted tissues enduring may respond transcriptionally to the stress.

Supercoiling lowers the free energy of DNA looping in a protein-dependent manner

Once the loop closes the DNA is partitioned into different topological domains. Previous work from our lab demonstrates that the lambda CI loop serves as a barrier for supercoiling diffusion (25), and work in this paper shows that LacI behaves similarly. Key features of this interplay are that supercoiling can become sequestered within a loop, but also that supercoiling modulates the looping probability (26). Supplementary Figure S6 is a plot of the energy change between looped and unlooped states under different supercoiling densities. Both positive and negative supercoiling lowered the free energy of LacI-mediated loop formation, but negative supercoiling was more effective. In addition, the response of different loop-mediating proteins, LacI and CI, is different. The free energy dropped more rapidly for LacI-mediatedlooping as negative supercoiling increased. This may reflect different binding interfaces with DNA, or their structures which may have different tolerances for changes in binding site phasing.

Comparing the effects of HU and supercoiling on DNA looping via the J factor

The J factor is a succinct parameter for comparing the effects of HU and supercoiling on DNA looping. It represents the effective concentration driving the binding of a protein at one site along a DNA molecule while simultaneously bound to another site along the same DNA tether. This factor accounts for the energy changes involved in forming a DNA loop independently of the affinity of protein linkages. The J factor can be calculated (10) from the ratio of the unlooped and looped state probabilities, $\frac{P_{\text{unloop}}}{P_{\text{loop}}}$, the dissociation constant from the secondary operator, $K_d$, and the concentration of lac repressor, [LacI], using the equation $J = 2 \frac{P_{\text{unloop}}}{P_{\text{loop}}} ([\text{LacI}] + K_d)$ (10). Increasing the HU concentration surrounding torsionally relaxed DNA tethers drove $J$ factors to plateau at 11–15 times the initial values, and slight tension reversed the gains (Figure 4A). In contrast, supercoiling, especially negatively, increased $J$ factors by several orders of magnitude from far below the free LacI concentration (1 nM), for which there was no looping under tension. Negative supercoiling drove the concentration of lac repressor binding sites to extremely high levels corresponding to $J$ factors far greater (effectively infinite) than those reported for a 400 bp loop in vivo (Figure 4B; purple dashed line). This produced perpetual loops which were not observed with HU protein alone even in tethers under no tension.

contraction to 0.7 of the torsionally relaxed extension were 100% looped for all three levels of tension tested.
CONCLUSION

Although HU binding promoted the formation of 400 bp, LacI-mediated loops in DNA molecules without tension, supercoiling was essential to drive significant looping of molecules under slight tension. While direct measurements of tension in genomic DNA have not been reported, the mechanical fact that DNA translocases can operate against as much as tens of pN of tension and the tension sensitivity of looping described above suggest that supercoiling is critical for looping in vivo. Simultaneously, a cellular perspective of the prominent role that protein-mediated loops play in chromatin condensation and transcriptional regulation, and the ubiquitous genetic requirement for topoisomerases that regulate supercoiling, reveal the importance of supercoiling in DNA biochemistry. Indeed, supercoiling directly reflects the current state of cellular metabolism and is a fundamental genomic parameter. Future studies are likely to show that, similarly to proteins that act at very specific sites, supercoiling can be constrained within loops and plec teuomes to control dispersion and locally regulate DNA transactions.

SUPPLEMENTARY DATA

Supplementary Data are available at NAR online.

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