Laboratory Search for a Long-Range $T$-Odd, $P$-Odd Interaction from Axionlike Particles Using Dual-Species Nuclear Magnetic Resonance with Polarized $^{129}$Xe and $^{131}$Xe Gas

M. Bulatowicz, R. Griffith, M. Larsen, and J. Mirijanian
Northrop Grumman Corporation, Woodland Hills, California 91367, USA

C. B. Fu, E. Smith, W. M. Snow, and H. Yan
Indiana University, Bloomington, Indiana 47408, USA

Center for Exploration of Energy and Matter, Indiana University, Bloomington, Indiana 47408, USA

T. G. Walker*
University of Wisconsin, Madison, Wisconsin 53706, USA

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Various theories beyond the standard model predict new particles with masses in the sub-eV range with very weak couplings to ordinary matter. A new $P$-odd and $T$-odd interaction between polarized and unpolarized nucleons proportional to $\vec{K} \cdot \vec{r}$ is one such possibility, where $\vec{r}$ is the distance between the nucleons and $\vec{K}$ is the spin of the polarized nucleon. Such an interaction involving a scalar coupling $g_s$ at one vertex and a pseudoscalar coupling $g_p$ at the polarized nucleon vertex can be induced by the exchange of spin-0 bosons. We used the NMR cell test station at Northrop Grumman Corporation to search for NMR frequency shifts in polarized $^{129}$Xe and $^{131}$Xe when a nonmagnetic zirconia rod is moved near the NMR cell. Long ($T_2 \sim 20$ s) spin-relaxation times allow precision measurements of the NMR frequency ratios, which are insensitive to magnetic field fluctuations. Combined with existing theoretical calculations of the neutron spin contribution to the nuclear angular momentum in xenon nuclei, the measurements improve the laboratory upper bound on the product $g_s^2 g_p^2$ by 2 orders of magnitude. The sensitivity of this technique can be increased by at least two more orders of magnitude.

The possible existence of new interactions of nature with ranges of macroscopic scale (millimeters to microns) and very weak couplings to matter was suggested long ago [1,2] and has recently begun to attract more scientific attention. Particles which might transmit such interactions are starting to be referred to generically as weakly interacting sub-eV particles [3]. Many theories beyond the standard model possess extended symmetries which, when broken at a high energy scale, produce pseudo-Nambu-Goldstone bosons and lead to weakly coupled light particles with relatively long-range interactions such as axions, familons, and Majorons [4]. Several attempts to explain dark matter and dark energy also produce new weakly coupled long-range interactions. The fact that the dark energy density of $O(1$ meV$^4$) corresponds to a length scale of 100 $\mu$m encourages searches for new phenomena around this scale [5,6].

Long ago, Moody and Wilczek [7] considered the form of interactions which could be induced by the exchange of a spin-0 field between fermions with scalar or pseudoscalar couplings. They highlighted an interesting $P$ and $T$ violating scalar-pseudoscalar (monopole-dipole) interaction of the form

$$ V = h^2 g_s g_p \frac{\hat{\sigma} \cdot \hat{r}}{8 \pi m} \left( \frac{1}{r^3} + \frac{1}{r^7} \right) e^{-r/\lambda}, $$

where $m$ is the mass and $K = h \hat{\sigma}/2$ is the spin of the polarized particle, $\lambda$ is the interaction range, $\hat{r} = r/r$ is the unit vector between the particles, and $g_s$ and $g_p$ are the scalar and pseudoscalar coupling constants. Axions [8], axionlike particles [3] predicted by string theory [9], or a very light spin-1 boson [10], can induce such an interaction and are candidates for cold dark matter [11]. The axion mass is constrained to the so-called “axion window” [6] between 1 $\mu$eV and 1 meV, corresponding to a range between 2 cm and 20 $\mu$m. Most experiments that have searched for such interactions [12–17] are sensitive to ranges $\lambda \lesssim 1$ cm.

Recent experimental work to constrain the monopole-dipole interaction at shorter distances has employed ultracold neutron bound states [18,19], polarized ultracold neutrons in material traps [20,21], and spin relaxation of polarized nuclei [22–25], with the most stringent direct experimental constraint on the product $g_s^2 g_p^2$ involving the neutron pseudoscalar coupling $g_p^n$ coming from NMR measurements on polarized $^3$He [25,26]. Torsion balance measurements recently set new stringent limits on possible monopole-dipole interactions involving polarized electrons [27]. Although all of these laboratory results are less stringent than those inferred from separate limits on $g_s$ and $g_p^n$ through a combination of torsion balance experiments and astrophysical constraints from stellar evolution.
and SN 1987A [28], laboratory experiments are more direct and therefore are of fundamental interest.

We used a NMR cell test station at Northrop Grumman Corporation, developed to evaluate dual species xenon cells for a gyroscope, to search for NMR frequency shifts in polarized $^{129}$Xe and $^{131}$Xe from the monopole-dipole interaction when a zirconia rod is moved near the NMR cell. By comparing the simultaneous frequencies of the two Xe isotopes, magnetic field changes are distinguished from frequency shifts due to the monopole-dipole coupling of the polarized Xe nuclei to the zirconia rod. We use calculations [29,30] of the neutron spin contribution to the nuclear angular momentum in $^{129}$Xe and $^{131}$Xe to put a new upper bound on the product $g_N g_p^n$ for ranges at the millimeter scale.

The NMR measurements use a magnetically shielded Pyrex comagnetometer cell consisting of $^{85}$Rb, 5 Torr $^{129}$Xe, 45 Torr $^{131}$Xe, and 250 Torr $^2$N$_2$. Figure 1 depicts the apparatus. The Rb atoms are spin polarized by absorption of circularly polarized light from a 795 nm, 50 mW pump diode laser and, through spin-exchange collisions, polarize the Xe nuclei parallel to a dc magnetic field [31]. The Rb atoms also serve as a magnetometer that detects the precession of the two xenon isotopes; the transverse magnetic fields of the polarized nuclei produce an oscillating transverse spin polarization of the Rb atoms that is detected as a rotation of the polarization of the linearly polarized sense laser.

We record simultaneous free-induction-decay (FID) signals from the Xe nuclei (Fig. 1). We initiate the FIDs by applying short resonant $\sim \pi/4$ pulses to rotate the two Xe polarizations away from the $\hat{z}$ direction. We isolate a single species FID by taking the raw FID, Fourier transforming it, applying a 10 Hz bandpass filter centered at the resonance frequency (152 Hz for $^{129}$Xe, 45 Hz for $^{131}$Xe), and inverse transforming it. We eliminate the first 1.6 sec and the last 0.2 sec of this signal, which contain filter artifacts and pulse residuals. Over the 100 sec FID acquisition time, there are Zeeman frequency drifts that arise from alkali polarization drifts and actual magnetic field noise. We use the $^{129}$Xe signal as our magnetometer for isolating these effects, fitting the $^{129}$Xe FIDs to the form $S_1 = A \cos(\alpha(t) + \phi_1) e^{-i t/\tau_2}$, where $\alpha(t) = 2 m |\gamma_1| t \int_0^t B(t') dt'$, and $\gamma_1$ is the gyromagnetic ratio. We use the deduced magnetic field $B(t)$ as input for the fits to the $^{131}$Xe FIDs to infer the $^{131}$Xe frequency $f_2$ as described in more detail below.

We performed the $g_N g_p^n$ search by comparing the ratios $f_1/f_2$ when a mass was close to or far away from the cell. To this end we attached a mounting structure to the magnetic shielding (dc shielding factor $= 3 \times 10^9$) to allow the repeatable positioning of a zirconia rod either 750 $\pm$ 60 $\mu$m or 1.0 $\pm$ 0.1 cm from the inner surface of the cell. The cell was a 1.9 mm internal dimension cube with a 0.5 mm diameter fill stem pinch-off on one side and 0.55 mm thick walls. The rod position was alternated for successive runs, with the time from the start of one run to the start of the next being about 2 min (4–5 relaxation times). Either the pump light polarization or the magnetic field direction was reversed every 10th run, and the magnitude of the magnetic field was changed once, from 0.13 to 0.064 G.

The $K = 1/2$ $^{129}$Xe isotope couples only to vector fields such as the external magnetic field, whereas the $K = 3/2$ $^{131}$Xe isotope also experiences quadrupole interactions with the electric field gradients on the cell walls. The nuclear spin Hamiltonian for $^{129}$Xe ($j = 1$) and $^{131}$Xe ($j = 2$) is

$$H_j = h \gamma_j B_j K_z + h X_j K_z + \delta_{j,2} H_Q. \quad (2)$$

There are four NMR frequencies deduced from the FIDs: $f_1 = |\gamma_1| B_1 + \hat{z} \cdot \hat{B} X_1$, $f_2 = |\gamma_2| B_2 + \hat{z} \cdot \hat{B} X_2 + q_i$, where the gyromagnetic ratios of species $j$ are $\gamma_j$, the monopole-dipole couplings are $X_j$, and the quadrupole shifts of the three NMR lines of $^{131}$Xe are $q_i$ ($i = -1, 0, 1$). The presence of the three frequencies is evident in the unusual shape of the $^{131}$Xe FID in Fig. 1. The two Xe isotopes may experience slightly different magnetic fields $B_j$ due to different interactions with the polarized Rb atoms. In previous experimental work using NMR of $K = 3/2$ nuclei [32–34], quadrupole interactions were treated in a spherical

![FIG. 1 (color online). Dual-species free-induction-decay (FID) spectrometer. A 2 mm glass cell containing $^{129}$Xe and $^{131}$Xe polarized by spin-exchange optical pumping of $^{85}$Rb is in a uniform magnetic field inside a magnetic shield. A movable zirconia rod enters from one end of the apparatus and the pump and sense lasers enter from the opposite side. FID signals of the Xe isotopes are sensed optically using the Rb vapor as a magnetometer. Sample FIDs, with fits, show $^{129}$Xe above, $^{131}$Xe below. For display purposes, the FID oscillations are down-converted to about 0.3 Hz from 152 or 45 Hz.](102001-2)
approximation. Our cell is cubic but the six internal surfaces are not identical, and the glass stem is located on one of the cell faces whose normal is along the y direction. The averaged quadrupole interaction on a surface with normal \( \mathbf{n} \) is \( V_q = Q_n (\mathbf{K} \cdot \mathbf{n} - \mathbf{K} \cdot \mathbf{K} / 3) / 2 \) [35]. We therefore consider the quadrupole interaction as a sum of contributions from each of the orthogonal faces of the cell. Second order perturbation theory shows that the three resonance frequencies in the \(^{131}\)Xe free-induction decay are

\[
f_{2i} = |\gamma_2 B_x| - \hat{z} \cdot \hat{B} X_2 + 2i |Q_\parallel| + \frac{3Q_1^2 \delta_0}{4f_2},
\]

where \( Q_\parallel = Q_z - (Q_x + Q_y)/2 \) and \( Q_\perp = Q_x - Q_y \). The first and second order quadrupole shifts are typically 20 mHz and 500 \( \mu \)Hz, respectively. By taking the average

\[
f_2 = \frac{f_{21} + f_{2-1}}{2} = |\gamma_2 B_x| - \hat{z} \cdot \hat{B} X_2,
\]

the quadrupole interaction is cancelled to second order. We therefore fit the \(^{131}\)Xe FIDs to

\[
S_2 = \sum_i A_i e^{-t/T_2} \cos \left( \frac{f_2}{f_1} \alpha_1 (t) + 2 \pi (f_{2i} - f_2) t + \phi_{2i} \right),
\]

with the quadrupole shifts and the frequency ratio being the fit parameters of primary interest.

The magnetic field experienced by the two nuclei is not only the applied field, but contains an additional fit parameters of primary interest.

This signals the presence of a slight isotopic difference in the light polarization and the magnetic field direction. In Fig. 2, we observe a small shift in the frequency ratio that is correlated with the product of the magnetic field direction and the polarization direction, as expected for a differential alkali field shift. The modulation doubles, as expected, when the magnetic field is halved at run 605, but a 1.5 ppm shift in the ratio of gyromagnetic ratios is also observed, as indicated by the thin solid green lines.

Figure 3(a) shows the full sequence of frequency ratio measurements, corrected for the differential alkali field shift and the observed shift when the magnitude of the magnetic field was halved. The data were taken over 4 days, with varying degrees of magnetic noise and optimization of magnetometer signals accounting for variations in the noise levels. About 70 runs were discarded due to rapid magnetic field variations that our fitting was not able to account for, or rapidly varying alkali field shifts that were probably due to laser instabilities, especially in the set of runs shortly after run 200. We fit the corrected frequency ratio data to the function \( \varrho + \hat{z} \cdot \hat{B} X / f_2 \) [Fig. 3(b)] with the ratio of gyromagnetic ratios \( \varrho \) and the weighted monopole-dipole shift \( X = X_1 + \varrho X_2 \). The mean of the gyromagnetic ratios at the two field strengths is \( \varrho = 3.373407 \pm 0.000002 \) (5), and \( X = 1.7 \pm 0.1 \) \( \mu \)Hz. The value of \( \varrho \) is consistent with Brinkmann [37], who found 3.37340(4) and observed a pressure dependence. We measured only one cell and have no information about pressure effects, so our value of \( \varrho \) should be considered specific to the parameters of our
cell. It may also be affected by an imperfect model for the quadrupole interaction.

To use $X$ to set a limit on the monopole-dipole interaction, we write Eq. (1) as $V = \nu(r)\langle \sigma_v \rangle$, giving $hX_i = \langle \nu(r) \rangle_{\text{vol}} (\langle \sigma_v \rangle_i / K_i)$. The volume average $\langle \nu(r) \rangle_{\text{vol}}$ over the polarized xenon and unpolarized zirconia (nucleon density $3.6 \times 10^{24}$ cm$^{-3}$) mass distributions is done numerically. The spin expectation values require knowledge of the neutron and proton angular momentum distributions of $^{129}$Xe and $^{131}$Xe. Such calculations have been done in the context of experimental searches for dark matter spin-flip scattering in liquid xenon. All calculations confirm that the spin of these even-Z nuclei almost entirely comes from the neutrons, so we interpret our results in terms of neutron coupling. In particular, the Bonn A calculations, in good agreement with recent effective field theory analysis of Menendez et al., give $(K_{130}^n) = -0.359$, $(K_{129}^p) = 0.028$, $(K_{131}^n) = -0.227$, and $(K_{131}^p) = -0.009$, and $g = 3.065$. These numbers give $hX = 0.51\langle \nu(r) \rangle_{\text{vol}}$.

Figure 4 shows how our upper limit on $X$ results in a limit on the monopole-dipole coupling strength as a function of the range $\lambda$. It excludes the light gray area in the $(g_s g_p^n, \lambda)$ plane. The limits shown involve the pseudoscalar coupling $g_p^n$ of the neutron and the scalar coupling $g_s$ of an ensemble of unpolarized matter made of a roughly equal proportion of neutrons, protons, and electrons. Our bounds $g_s g_p^n \leq 10^{-18}$ for $\lambda = 0.1$ mm to $g_s g_p^n \leq 2 \times 10^{-24}$ for $\lambda = 1$ cm are the most stringent laboratory limits over these distances, which correspond to exchange boson masses from $10^{-3}$ to $10^{-5}$ eV/c$^2$.

There is great room for improvement of the measurement sensitivity using this technique. Direct stabilization of the $^{129}$Xe frequency using magnetic field feedback, plus stabilization of the alkali magnetization, would likely reduce the statistical uncertainties by 1–2 orders of magnitude and lower the limits on $g_s g_p^n$ correspondingly. Improvement of the magnetic field shielding and making NMR oscillators would yield additional sensitivity improvements.

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Note added.—Reference [40] reports improved limits on $g_s g_p^n$ at distances longer than 0.5 mm.

*tgwalker@wisc.edu

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