Flavour Violating Axions

Luca Di Luzio

1 Deutsches Elektronen-Synchrotron DESY, Notkestraße 85, D-22607 Hamburg, Germany

Abstract. I review the physics case for flavour violating axions. In particular, I argue that relaxing the assumption of the universality of the Peccei-Quinn current opens up new pathways, including: the relaxation of the Supernova bound on the axion mass, a possible connection with the Standard Model flavour puzzle and the experimental opportunity of discovering the axion via flavoured axion searches.

1 Introduction

Axion physics has entered a new, experimentally driven phase. In the recent years we have witnessed the emergence of several new experimental proposals, which (in different stages of development) promise to open for exploration regions of parameter space considered unreachable until few years ago (for recent overviews see Refs. [1, 2]). It is hence timely, on the theory side, to reassess axion properties beyond standard scenarios. In this contribution, I first review some basics aspects of axion physics. The emphasis is put on the fact that axion couplings are inherently UV dependent, so that a wide experimental program should keep this into account, regardless of theoretical prejudice. In particular, I will focus on a commonly adopted, although not strongly motivated, assumption which consists in the universality of the Peccei-Quinn (PQ) current. I will argue, both with old examples and more recent ones, that relaxing the latter assumption is motivated by various phenomenological and theoretical arguments. Most importantly, it offers a unique experimental handle which consists in flavour-violating (FV) axion transitions. The latter turn out to be complementary to standard axion searches and potentially competitive with astrophysical bounds.

2 Axion couplings: model-independent vs. model-dependent

The essence of the axion solution of the strong CP problem is a new spin-0 field \( a(x) \), the axion, endowed with a pseudo-shift symmetry \( a \rightarrow a + \alpha f_a \) that is broken only by the operator

\[
\frac{a}{f_a} a\frac{\partial}{\partial x} G G^* .
\]  

While the QCD \( \theta \) term can be rotated away via an appropriate choice of \( \alpha \), a Vafa-Witten theorem [3] ensures that in a vector-like theory such as QCD, \( E((a) = 0) \leq E((a) \neq 0) \), thus solving the strong CP problem. The origin of the \( aG\bar{G} \) operator in Eq. (1) can be traced back in the existence of a QCD-anomalous, global \( U(1)_{\text{PQ}} \) symmetry, whose spontaneous breaking delivers the axion as a pseudo-Nambu-Goldstone boson.

The \( aG\bar{G} \) operator represents the smoking-gun signature of the PQ mechanism and determines the so-called model-independent properties of the axion field, which are given solely in terms of the axion decay constant \( f_a \). These are the axion mass \( m_a = 5.691(51) \mu eV \left( 10^{12} \text{GeV}/f_a \right) [4] \), and the axion couplings to photons, nucleons and electrons (here we focus on the most relevant ones for astrophysical limits), arising from the diagrams in Fig. (1).

Given the effective axion Lagrangian

\[
\mathcal{L}_a \supset \frac{a}{8\pi} \frac{C_\gamma}{f_a} a F \tilde{F} + \frac{C_f}{2f_a} \partial_\mu a \tilde{\gamma}^\mu \gamma f , \quad (f = p, n, e),
\]  

the numerical values of the coefficients \( C_\gamma, p, n, e \) can be determined via chiral Lagrangian techniques, as well as inputs from Lattice QCD, and they are found to be [5–7]

\[
C_\gamma = -1.92(4), \quad C_p = -0.47(3), \quad C_n = -0.02(3), \quad C_e = -7.8(2) \times 10^{-6} \log \left( \frac{f_a}{m_e} \right) .
\]
However, being the description of the effective operator in Eq. (1) valid only until energies of the order of $f_a$, the theory must be UV completed. Remarkably, the UV completion of the axion effective Lagrangian can drastically affect the low-energy properties of the axion, and hence the way to experimentally probe it. There are basically two main ways in which this can happen, as depicted schematically in the diagrams of Fig. (2).

Figure 2. Model-dependent axion couplings to photons and SM quarks and leptons.

In the left diagram of Fig. (2), the PQ-charged colored fermions responsible for generating the $aG\bar{G}$ operator can also lead to a direct QED-anomalous contribution to $aFF$, if the new fermions they are charged under $U(1)_{\mathbb{P}Q}$. Then the axion coupling to photons gets modified into $C_r = E/N - 1.92(4)$, where $E/N$ is a group theory factor which depends on the quantum numbers of the fermions running in the loop (see e.g. Refs. [8, 9] for phenomenologically motivated ranges of $E/N$).

The other possibility, depicted in the right diagram of Fig. (2), is that the axion interacts directly with the Standard Model (SM) fermions, which are charged under the $U(1)_{\mathbb{P}Q}$. In this case, the axion effective interaction can be written as (keeping for the sake of illustration only SM quarks)

$$\frac{\partial_\mu a}{v_{\mathbb{P}Q}} = \frac{\partial_\mu a}{v_{\mathbb{P}Q}} \times \left[ -\tilde{Q}_L^\ast X_{Q,\gamma'}_L - \tilde{u}_R X_{u\gamma_j} u_R - \tilde{d}_R X_{d_i \gamma_i} d_R \right],$$

where $f_{\mathbb{P}Q}$ is the conserved (up to anomalies) PQ current, depending on the $U(1)_{\mathbb{P}Q}$ charges. The latter are denoted by $X_{Q,\gamma_i u_R d_L}$, which are diagonal (in general, non-universal) matrices. After going to the mass basis: $u_L \rightarrow V_{u_i} u_i$, etc., and using the relation $f_a = v_{\mathbb{P}Q}/(2N)$ between the axion decay constant and the PQ-breaking order parameter, we can recast Eq. (4) as

$$\frac{\partial_\mu a}{2f_a} \psi_i (C_{\mathbb{P}Q}^{\psi_i | \phi} + C_{\mathbb{P}Q}^{\psi_i | \gamma_i}) \gamma^\mu \psi_j,$$

where mass eigenstates are denoted as $\psi_i = [u_i, d_i]$, and we have introduced the vector and axial couplings

$$C_{u_i u_j}^{\mathbb{P}Q} = \frac{1}{2N} \left( V_{u_i}^{\dagger} Y_Q V_{u_j} \pm V_{u_i}^{\dagger} X_{\gamma_i} V_{u_j} \right),$$

$$C_{d_i d_j}^{\mathbb{P}Q} = \frac{1}{2N} \left( V_{d_i}^{\dagger} Y_Q V_{d_j} \pm V_{d_i}^{\dagger} X_{\gamma_i} V_{d_j} \right),$$

Note that the unitary flavour matrices are only subject to the constraint $V_{\mathbb{K}M} = V_{\mathbb{K}M}^\dagger$.

A common assumption, as e.g. in the original Peccei-Quinn-Weinberg-Wilczek (PQWW) [10–13] and the Dine-Fischler-Srednicki-Zhitnitsky (DFSZ) [14, 15] axion models, consists in the universality of the PQ current, i.e. $X_{Q,\gamma_i u_R d_L} \propto v_i$. This implies flavour blind axion interactions: the axion interacts in the same way with SM fermions having the same gauge quantum numbers and, moreover, off-diagonal entries in Eq. (5) trivially vanish.

### 3 A lesson from flavour

The simplest axion model featuring only two Higgs doublets for the breaking of the $U(1)_{\mathbb{P}Q}$, also known as PQWW model, was ruled out quite soon after its conception, due to a combination of beam dump experiments and rare meson decays such as $K \rightarrow \pi a$ [18] and Quarkonia $\rightarrow \gamma a$ [19]. For instance, radiative decays of Quarkonia to $\gamma a$ normalised to leptonic modes can be written at the leading order as [19]

$$\frac{\mathbb{B}(J/\psi \rightarrow \gamma a)}{\mathbb{B}(J/\psi \rightarrow \mu \mu)} = \frac{g_{\gamma}^2}{2\pi}, \quad \frac{\mathbb{B}(\Upsilon \rightarrow \gamma a)}{\mathbb{B}(\Upsilon \rightarrow \mu \mu)} = \frac{g_{\gamma}^2}{2\pi},$$

where $g_{\gamma} = m_c C_{cc} / f_a$ (in the notation of Eq. (5)) and similarly for $g_{\mu}$. In the PQWW model one has

$$g_{\gamma} = m_c \frac{1}{v \tan \beta}, \quad g_{\mu} = m_s \frac{v}{\tan \beta},$$

with $v = 246$ GeV and $\tan \beta = \langle H_u \rangle / \langle H_d \rangle$. Since the couplings in Eq. (9) cannot be simultaneously suppressed, bounds from Quarkonia alone would have been sufficient to rule out the PQWW model (for a historical account see Sect. 3 in Ref. [20]).

However, a main assumption behind the PQWW model consisted in the universality of the PQ current. At the beginning of the 80’s it seemed more natural to keep this assumption, and extend the model by adding a SM-singlet field in order to decouple the PQ breaking from the electroweak scale. Models of this type became known as invisible axion models and led to the standard KSVZ/DFSZ benchmarks. In the same years, the GSI anomaly [21–23] (a sharp peak in the $e^+e^-$ spectrum of heavy ion collisions) which could be interpreted in terms of an $O$(MeV) axion with dominant decay mode $a \rightarrow e^+e^-$, triggered a lot of interest in trying to explain that in terms of variant axion models, with a non-universal axion mainly coupled to first generation fermions in order to avoid bounds from Quarkonia decays. It actually took almost a decade, starting from the original PQWW proposal, to rule out non-universal PQWW variants, by combining informations from rare $\pi$ and $K$ decays [24]. Even nowadays, there is an interesting claim that under certain

\[ \text{We remind the reader that instead in Kim-Shifman-Vainshtein-Zakharov (KSVZ) [16, 17] type of models the SM fields are not charged under the $U(1)_{\mathbb{P}Q}$.} \]

\[ \text{On the contrary, it can be argued that imposing $f_a \gg v$ leads to two well-known naturalness issues: the hierarchy problem and the PQ-quality issue.} \]
conditions (among which the non-universality of the PQ current) an $O$(MeV) axion is not obviously ruled out [25].

4 Non-universal Peccei-Quinn axion models

We explore now some consequences of non-universal PQ axion models, focussing on some recent developments such as the possibility of suppressing the axion coupling to protons and neutrons (nucleophobia), which allows in turn to relax the Supernova (SN) bound on the axion mass. We next make some considerations on possible connections of non-universal PQ scenarios with the SM flavour puzzle and summarize the status of flavoured axion searches.

4.1 Nucleophobia

The axion coupling to nucleons (cf. Eq. (2)) can be computed using a non-relativistic effective field theory where nucleons are at rest and the axion is treated as an external current (see [5] for details). In particular, one obtains

\[ C_p + C_n = (c_u + c_d)(\Delta_u + \Delta_d) - 2\delta_5, \]  
\[ C_p - C_n = (c_u - c_d)(\Delta_u - \Delta_d), \]

where $c_{u,d}$ are derivative axion couplings to the axial current of valence quarks in the nucleon, defined in the basis where the $aGG$ has been rotated away (cf. Eq. (13)), $\delta_5 \approx 5\%$ encodes effects from sea quarks in the nucleon, and $\Delta_{u,d}$ are nucleon matrix elements which are extracted from experiments and/or the lattice. Hence, if we want to simultaneously suppress both the axion-nucleon couplings, say at the level of 10%, we need to impose $c_u + c_d = 0$ and $c_u - c_d = 0$, regardless of the specific value of $\Delta_{u,d}$.

It is instructive to see why achieving such cancellation is not possible in standard KSVZ and DFSZ models. Let us consider the axion Lagrangian in Eq. (4), restricted to first generation up and down quarks, and ignoring for the moment flavour mixing. Including also the $aGG$ term, the latter reads

\[ \mathcal{L}_a \supset \frac{\alpha}{f_a} \frac{\partial \varphi}{\partial \varphi} \left[ X_u \bar{u} \gamma^5 u + X_d \bar{d} \gamma^5 d \right] \]

where $2X_u \equiv X_{Q_1} - X_{u_1}$ and $2X_d \equiv X_{Q_1} - X_{d_1}$ are the PQ charges expressed in terms of the chiral ones (for notational simplicity, we have suppressed the chirality indices in the right-hand sides). The $aGG$ term can be rotated away via a field-dependent 2-flavour quark transformation: $q \rightarrow \exp(i\gamma_5 Q_a(a(x))(2f_a))q$, with $q = (u, d)^T$ and $Q_a = \text{diag}(m_d/m_u, m_u/m_d, m_d/m_u)$. The latter choice ensures that the axion has no mass mixing with the neutral pion [26]. In the new basis, Eq. (12) reads

\[ \mathcal{L}_a \supset \frac{\partial \varphi}{\partial \varphi} \left[ X_u \bar{u} \gamma^5 u + X_d \bar{d} \gamma^5 d \right]. \]

Hence, the nucleophobic conditions can be recast as

\[ 0 = c_u + c_d = \frac{X_u + X_d}{N} - 1, \]
\[ 0 = c_p - c_n = \frac{X_u - X_d}{N} - \frac{m_u}{m_u + m_d}, \]

While the second condition can always be implemented via a tuning (see below), the real bottleneck is the first one, since $X_u = X_d = 0$ in KSVZ models, while in DFSZ models one has $N = \frac{1}{2}n_f(2Q_{d_1} - Q_{u_1} - Q_{d_1})$ or $n_f(2X_u + X_d)$, with $n_f = 3$ denoting the number of families.

The above no-go theorem for standard axion models suggests itself a possible way out [27]: if the total anomaly factor were equal to that of the first family, i.e. $N = N_1 = X_u + X_d$, the first condition would be automatically satisfied. To simplify the discussion, let us assume a 2+1 structure such that the PQ charges of the first two generations are the same. Then the condition we would like to impose, $N \equiv N_1 + N_2 + N_3 = N_1$, simply implies $N_1 = N_2 = -N_3$. It is remarkably simple to obtain the latter in terms of a renormalizable Yukawa Lagrangian featuring two Higgs doublets $H_{1,2} \sim (1, 2, -1/2)$. For instance,

\[ \mathcal{L}_Y \supset \bar{Q}_u \mu H_1 + \bar{Q}_d \mu H_2 + \ldots + \bar{Q}_u \mu H_2 + \bar{Q}_d \mu H_1 + \ldots, \]

where we have suppressed Yukawa couplings and the dots stand for off-diagonal operators which are necessary in order to obtain a realistic CKM mixing, compatible the overall PQ charge assignments. Denoting by $X_{1,2}$ the PQ charges of $H_{1,2}$, from Eq. (16) we have $N_3 = \frac{1}{2}(2X_{Q_1} - X_{u_1} - X_{d_1}) = \frac{1}{2}(X_1 - X_2)$ and $N_2 = \frac{1}{2}(2X_{Q_1} - X_{u_1} - X_{d_1}) = \frac{1}{2}(X_2 - X_1)$, having swapped the role of $H_1$ and $H_2$ for the third and second/first generations. Hence, $N = N_1 = \frac{1}{2}(2X_{Q_1} - X_{u_1} - X_{d_1}) = X_u + X_d$ and Eq. (14) is automatically satisfied in terms of charge assignments.

Coming to the second nucleophobic condition in Eq. (15), this can be expressed as a condition on $\tan \beta = \langle H_2 \rangle / \langle H_1 \rangle$. In order to see that, let us first impose the orthogonality between the PQ and hypercharge currents: $Y(H_1)X_{1,2}^2 + Y(H_2)X_{2,1}^2 = 0$, and hence $X_1/X_2 = -\tan^2 \beta$, implying no kinetic mixing between the axion and the $Z$ boson. Using $X_u - X_d = \frac{1}{2}(X_{d_1} - X_{u_1}) = \frac{1}{2}(X_2 + X_1)$ and

\[ \frac{1}{2}(X_1 - X_2) \]

\[ \frac{1}{2}(X_2 - X_1) \]

\[ \tan \beta = \frac{\langle H_2 \rangle}{\langle H_1 \rangle}. \]

\[ \frac{1}{2}(X_2 + X_1), \]

This include as well a scalar potential communicating the PQ breaking to the two Higgs doublets via a SM singlet scalar, in a fashion similar to universal DFSZ models. In the absence of texture zeros and for a 2+1 structure for the PQ charges, all the possible Yukawa structures leading to nucleophobia have been classified in Ref. [27]. The opposite case of maximal numbers of texture zeros has been discussed instead in Ref. [28].
4.3 Flavoured axion searches

Rare FV decays with invisible and light final states allow to probe the off-diagonal axion couplings $C_{\phi ab}^{\alpha \beta}$ in Eq. (5). A collection of bounds can be found for instance in Refs. [47–49]. The strongest limits on FV axion couplings to quarks come from $K^+ \to \pi^* a$. Comparing the theoretical prediction with the current limit from E949/E787 [50] gives $m_a < 2 \times 10^{-5} \text{eV}/|C_{\phi ab}^{\alpha \beta}|$, which for maximal mixing (i.e. $C_{\phi ab}^{\alpha \beta} = O(1)$) is about three orders of magnitude stronger than typical astrophysical bounds. Hence, $K^+ \to \pi^* a$ clearly provides a golden channel for FV axion searches.\textsuperscript{10} NA62 is expected to improve the limit on $B(K^+ \to \pi^* a)$ by a factor of ~70 [51, 52], thus strengthening the axion mass bound by a factor ~8. The next most sensitive process in the quark sector is $B^+ \to K^* a$, whose present limit from CLEO [53] corresponds to $m_a < 9 \times 10^{-2} \text{eV}/|C_{\phi ab}^{\alpha \beta}|$, close to astrophysical limits for maximal mixing. This latter bound could be presumably strengthened by a factor ~10 at BELLE II [54]. A similar, but slightly weaker bound, is obtained for $B^+ \to \pi^* a$, which involves the coupling $C_{\phi ub}^{\alpha \beta}$. On the other hand, bounds on processes involving other quark transitions are about three orders of magnitude smaller (see Table 2 in Ref. [48]), and hence not competitive with astrophysical limits, even for maximal mixing. In the charged lepton sector, the strongest limits come from (30 years old) searches for $\mu \to e\nu\gamma$ [55, 56]. They yield $m_a < 3 \times 10^{-3} \text{eV}/(|C_{\phi ub}^{\alpha \beta}|^2 + |C_{\phi sd}^{\alpha \beta}|^2)^{1/2}$, competitive with astrophysical bounds in the case of sizeable flavour mixing. This bound is likely to be improved by one order of magnitude at the MEG [57] and Mu3e [58] experiments at PSI. On the other hand, bounds on $\tau$-$\mu$ and $\tau$-$e$ transitions from ARGUS [59] yield axion mass limits which are still well-below astrophysical ones.

5 Conclusions

Relaxing the assumption of the universality of the PQ current opens up the parameters space of DFSZ models, by

$\textsuperscript{4}$The level of tuning useful for nucleophobism is limited by the remainder $2\beta \approx 10\%$ in Eq. (10), which sets an irreducible contribution to nucleon couplings. In principle, flavour mixing (neglected in the present simplified discussion) also enters diagonal axion couplings when going to the mass basis (cf. Eqs. (6)–(7)), and cannot be used to further cancel the $\phi$ contribution [27].

$\textsuperscript{5}$Having a sizeable $g_{uv}$ with a somewhat relaxed SN bound improves the fit of the cooling anomalies [32].

$\textsuperscript{6}$Gauging the horizontal flavour group can also lead to an accidental global $U(1)$ whose spontaneous breaking delivers a flavoured axion [39] or a flavoured axion [40–42].

$\textsuperscript{7}$Up to the usual dependence from $f_a$ and $\tan\beta$, as in universal DFSZ models.

$\textsuperscript{8}$It should be noted that pseudo-scalar meson decays such as $K \to \pi a$ are sensitive only to the vectorial part of the quark current, since $\langle \pi|\bar{q}_\mu(q_\mu)d(K)\rangle = 0$ by the Wigner-Eckart theorem. In order to set bounds on $C_{\phi ab}^{\mu \nu}$ one has to resort to other FV processes, as for example $K^0 - \bar{K}^0$ mixing, which however are much weaker compared to the limits on the vectorial counterpart from meson decays. In principle, this would leave open a possibility in order to evade the strong constraints from $K \to \pi a$ in the presence of large mixing, if one could cook up a model with $C_{\phi ab}^{\mu \nu} \sim C_{\phi ab}^{\nu \mu}$.
introducing 34 new real parameters only in the quark sector (most of which are related to the diagonalizing U(3) matrices in Eqs. (6)–(7)). These new parameters arise, in some sense, within the SM (since they come from the diagonalization of the Yukawas that we write in the SM Lagrangian), but the SM is “blind” to them. By extending the SM with the axion at low-energy, it is somewhat artificial to require that flavour mixing beyond the CKM is unphysical and we should rather let experiments to decide. In the meanwhile, it is worth to speculate about the possible consequences of the non-universality of the PQ current, as I have done in the present contribution.

To conclude, I cannot resist from making an unfortunate analogy: “DFSZ = cMSSM”. The DFSZ model corresponds, in some sense, to the constrained version of the MSSM with universal soft terms. There is however an important difference, while large flavour violating effects in low-energy SUSY were often considered as a curse (flavour problem), in the case of the axion they rather come as a blessing (flavour opportunity).

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