Elemental Abundances in M31: Individual and Coadded Spectroscopic [Fe/H] and [$\alpha$/Fe] throughout the M31 Halo with SPLASH

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Abstract

We present spectroscopic chemical abundances of red giant branch stars in Andromeda (M31), using medium-resolution ($R \sim 6000$) spectra obtained via the Spectroscopic and Photometric Landscape of Andromeda’s Stellar Halo survey. In addition to individual chemical abundances, we coadd low signal-to-noise ratio spectra of stars to obtain a high enough signal to measure average [Fe/H] and [$\alpha$/Fe] abundances. We obtain individual and coadded measurements for [Fe/H] and [$\alpha$/Fe] for M31 halo stars, covering a range of 9–180 kpc in projected radius from the center of M31. With these measurements, we greatly increase the number of outer halo ($R_{\text{proj}} > 50$ kpc) M31 stars with spectroscopic [Fe/H] and [$\alpha$/Fe], adding abundance measurements for 45 individual stars and 33 coadds from a pool of an additional 174 stars. We measure the spectroscopic metallicity ([Fe/H]) gradient, finding a negative radial gradient of $-0.0084 \pm 0.0008$ for all stars in the halo, consistent with gradient measurements obtained using photometric metallicities. Using the first measurements of [$\alpha$/Fe] for M31 halo stars covering a large range of projected radii, we find a positive gradient ($+0.0027 \pm 0.0005$) in [$\alpha$/Fe] as a function of projected radius. We also explore the distribution in [Fe/H]–[$\alpha$/Fe] space as a function of projected radius for both individual and coadded measurements in the smooth halo, and compare these measurements to those stars potentially associated with substructure. These spectroscopic abundance distributions add to existing evidence that M31 has had an appreciably different formation and merger history compared to our own Galaxy.

Unified Astronomy Thesaurus concepts: Stellar abundances (1577); Stellar streams (2166); Galaxy stellar halos (598); Andromeda Galaxy (39); Local Group (929)

1. Introduction

The stellar halos of late-type galaxies contain a wealth of information detailing the formation and merger history of the host galaxy. The earliest models of halo formation followed two distinct pathways: rapid radial collapse (Eggen et al. 1962), and the accretion model (Searle & Zinn 1978). Modern halo formation scenarios follow cosmologically motivated prescriptions for hierarchical formation (e.g., Bullock & Johnston 2005), where galactic halos are built up through the accumulation of smaller satellites (Cole et al. 1994; Johnston et al. 1996; Bullock et al. 2001; Helmi 2008). These satellites are typically assimilated into the host galaxy, making it difficult to determine which stars were formed in situ, and which were formed in a galaxy that has since been accreted.

Our nearest spiral neighbor, the Andromeda galaxy (M31), offers a particularly illuminating case for understanding the stellar halo of a massive galaxy. Within its halo, we observe a kinematically hot classical halo component (e.g., Guhathakurta et al. 2005; Kalirai et al. 2006b), many distinct debris streams (e.g., Ibata et al. 2001, 2007; Zucker et al. 2004; McConnachie et al. 2009), ancient globular clusters (GCs; e.g., Mackey et al. 2019), and intact dwarf spheroidal galaxies (McConnachie 2012; see McConnachie et al. 2018 for a recent review of these components). In M31, accretion events where tidal debris has not yet been phased mixed can be identified as overdensities in star count maps (e.g., Ibata et al. 2001; Ferguson et al. 2002), and as kinematic peaks in the velocity distribution of the halo (e.g., Kalirai et al. 2006b; Gilbert et al. 2009). The largest and most massive of these features is the giant stellar stream (GSS; Ibata et al. 2001), which likely is the result of a recent (<4 Gyr ago) accretion of an $M_\star \sim 10^9–10^{10} M_\odot$ satellite galaxy (e.g., Fardal et al. 2013; D’Souza & Bell 2018; Hammer et al. 2018). In addition, it has been shown that a number of additional debris features in the halo of M31 may be related to this interaction (Fardal et al. 2006, 2007, 2008, 2012; Gilbert et al. 2007; Dey et al. 2023; Escala et al. 2022). These substructure features cover a large radial extent, and can be found out to a projected radius of $\sim 90$ kpc from M31’s center.
In our own Galaxy, 6D phase space information is now available for hundreds of thousands of individual stars (e.g., Abdurro’uf et al. 2022; Gaia Collaboration et al. 2022). In contrast, we rely on a significantly less-complete kinematical data set for stars in M31, where kinematical information for individual stars is typically limited to line-of-sight velocity measurements. However, abundance measurements are attainable for individual stars in M31, and can be obtained using either photometry or spectroscopy. Therefore, because it is directly measurable and not dependent on modeling missing dimensions for interpretation, at present it is most straightforward to utilize the chemical abundance information available from these M31 stars to reconstruct the evolutionary history of M31’s halo.

Metallicity and elemental abundance measurements are extremely informative with respect to exploring the star formation and assembly history of a galaxy. Hierarchical formation scenarios predict a spread in metallicity as a function of distance from the center of the galaxy, as accreted populations are likely to have a wide range of star formation histories that also differ from that of the host galaxy itself. Star formation and chemical enrichment timescales are typically driven by the mass of a system, and therefore the mass distribution, as well as time of accretion of accreted galaxies, imprint on the observed abundances in the host. Generally, cosmological models (e.g., Samland & Gerhard 2003; Kobayashi & Nakasato 2011; Grand et al. 2017; Tissera et al. 2017; Monachesi et al. 2019) predict metallicity gradients as a function of radial distance for disk and halo populations, as the inner regions are more dense and therefore have a higher star formation efficiency (reaching higher metallicities), compared to the outer regions, which are sparser and have lower rates of star formation.

In a similar vein, the distribution of the ratio of α-elements (e.g., Mg, Si, Ca, Ti) to Fe ([α/Fe]13) as a function of [Fe/H] directly correlates to the enrichment history of a system: stars that explode as Type II supernova produce α-elements and Fe. When Type Ia supernova begin to contribute their ejecta, which are much richer in Fe than α-elements, to the interstellar medium, the [α/Fe] ratio decreases as a function of increasing [Fe/H]. The position of the decrease in [α/Fe] is often referred to as a “knee” of the distribution, and where this knee falls as a function of [Fe/H] provides vital information on the star formation and enrichment history of the environment where those stars were formed. In low-mass galaxies, this “knee” is observed at lower values of [Fe/H] compared to higher-mass systems (McWilliam 1997; Tolstoy et al. 2009).

Compared to the MW, the halo of M31 is overall significantly more metal-rich for comparable radial ranges (Mould & Kristian 1986; Durrell et al. 1994; Rich et al. 1996). While the metal-rich nature of the M31 halo is well documented, measuring the presence (or lack thereof) of stellar metallicity gradients across the halo of M31 has required surveys over a substantial radial range, which has not been possible until relatively recently. Early work, restricted to limited ranges in projected distance from M31, found little evidence for a metallicity gradient. Using Canada–France–Hawaii Telescope (CFHT) photometry of individual stars, Durrell et al. (2001, 2004) found no evidence for a radial metallicity gradient out to 30 kpc. Ferguson et al. (2002) carried out a panoramic imaging study of M31 using the Wide Field Camera on the Isaac Newton Telescope, and while they found some variation in the color (and therefore metallicity) of red giant branch (RGB) stars as a function of position across the M31 halo, they did not find evidence for a gradient. In addition, Bellazzini et al. (2003) found “remarkably uniform” metallicity distributions of 16 fields observed with HST photometry out to a projected radius of 35 kpc.

These early results conflict with more recent photometric and spectroscopic studies that found evidence for a metallicity gradient in the M31 halo. The Pan-Andromeda Archaeological Survey (PAndAS; McConnachie et al. 2009) obtained comprehensive photometric coverage of the M31 halo out to ~150 kpc in projected radii from the center of M31. Studies using these data found evidence for low-metallicity stellar populations at large projected radii, based on comparing the position of stars in the color–magnitude diagram to stellar isochrones (Irwin et al. 2005; Chapman et al. 2006; Ibata et al. 2014). A number of other photometric surveys were conducted to explore evidence for a metallicity gradient in the halo of M31, with varying results (Richardson et al. 2009; Tanaka et al. 2010; see Gilmore et al. 2014 and references therein for a comprehensive history).

Using the DEIMOS instrument on the 10 m Keck II telescope, the Spectroscopic and Photometric Landscape of Andromeda’s Stellar Halo (SPLASH) survey obtained spectra for thousands of RGB stars throughout the disk, halo, and satellites of M31 (e.g., Dorman et al. 2012; Gilbert et al. 2012; Tollerud et al. 2012). With the first SPLASH fields, Kalirai et al. (2006b) found a significant metallicity gradient (with both CMD-based and Ca II triplet-based [Fe/H] estimates) using over 250 secure M31 member stars, observed with Keck/DEIMOS spectroscopy, from 12 fields spanning 12–165 kpc in projected radius from the center of M31. Gilbert et al. (2014) analyzed a much larger SPLASH halo sample (over 1500 individual RGB stars). They corroborated the presence of a large-scale metallicity gradient, using both photometric metallicity measurements and Ca II triplet-based metallicity measurements, for individual stars over a similar range (10–90 kpc) in projected radii. However, these prior metallicity measurements are all indirect measurements of [Fe/H] that rely on a significant number of assumptions, and do not provide estimates for [α/Fe]. Therefore, a substantial effort has been made to obtain spectral abundance measurements via spectral synthesis for both individual and coadded stars observed as part of SPLASH.

Vargas et al. (2014) presented the first spectroscopic abundance measurements in M31’s halo using SPLASH data, obtaining spectroscopic [Fe/H] and [α/Fe] abundances for four stars in the outer halo (70 < Rproj < 140 kpc) of M31. They found these outer halo stars to be metal-poor ([Fe/H] ~ −2.2 to −1.4), with an average [α/Fe] of 0.2 ± 0.2. Gilbert et al. (2020) added to this sample 21 outer halo stars with spectroscopic [Fe/H] measurements, and seven outer halo stars with both [Fe/H] and [α/Fe] abundance measurements. These outer halo stars were also measured to be relatively [α/Fe]-enhanced and metal-poor, and were found to be more similar to the outer halo of the MW than the inner halo of M31. Most recently, for a sample of stars in the inner regions (8 < Rproj < 34 kpc) of the M31 halo with spectra observed using long exposures with the 600ZD grating, Escala et al. (2020b) found a similar (−0.025 ± 0.002 dex kpc−1)

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13 Throughout the paper, we use the standard definition for elemental abundance ratios: \([X/H] = \log_{10}(N_X/N_H)_{\text{star}} - \log_{10}(N_X/N_H)_{\text{sun}}\).
spectroscopic [Fe/H] gradient, and a flat gradient in $[\alpha/Fe]$. Escala et al. (2021) also found the GSS to be $[\alpha/Fe]$-enhanced compared to the smooth halo, with a mean of $\sim0.4$ dex and a large spread in $[\alpha/Fe]$.

In this work, we greatly expand on previous spectroscopic abundance measurements ([Fe/H] and $[\alpha/Fe]$) in M31’s halo using the SPLASH halo sample of Gilbert et al. (2018), which includes fields covering a large radial extent (9–180 kpc) in projected radius from the center of M31. We measure both individual and coadded abundances: for M31 spectra without sufficient signal-to-noise ratio (S/N) to measure individual abundances, we coadd spectra to obtain an S/N high enough to measure mean [Fe/H] and $[\alpha/Fe]$ abundances (Yang et al. 2013; Wojno et al. 2020). In particular, we greatly improve the number of M31 stars with abundance measurements at large values of $R_{\text{proj}}$. For stars with $R_{\text{proj}} > 50$ kpc, we measure abundances for 45 individual stars, with another 174 stars represented in 33 coadds. Previously, only six stars in M31 contained a comprehensive summary of all relevant observational constraints for the data used in this study.

In Section 2.2, we describe the observation strategy and data reduction used to gather the spectra used in this work. To the wealth of analysis previously conducted with these data (e.g., Gilbert et al. 2012, 2014, 2018), we contribute spectroscopic measurements of [Fe/H] and $[\alpha/Fe]$ for individual stars (Section 3), as well as coadded abundances (Section 3.5), making use of stars that do not have secure individual abundance measurements. We present our measurements of the spectroscopic radial metallicity gradients in the halo of M31 in Section 4, both for [Fe/H] (Section 4.1), and for $[\alpha/Fe]$ (Section 4.2). We also explore the [Fe/H]–$[\alpha/Fe]$ abundance plane as a function of projected radius for both the smooth halo (Section 4.4) and stars potentially associated with known substructure components (Section 5). In Section 5, we show the [Fe/H]–$[\alpha/Fe]$ abundance distribution for each substructure component present in our sample. In Section 6, we explore origin scenarios for the radial abundance gradients that we find, as well as the unique abundance distribution of stars in the outer halo. Finally, Section 7 summarizes our findings.

2. Observations and Data

We use spectra of RGB stars in the halo of M31 obtained via the SPLASH survey. The SPLASH survey was conducted over the course of approximately 10 yr, collecting photometry and low- and medium-resolution spectra for $\sim10^3$ individual stars. We refer the reader to Gilbert et al. (2012, 2014, 2018) for full details on the data reduction, spectroscopic slitmask design, and survey strategy.\footnote{Table 1 of Gilbert et al. (2012) contains a comprehensive summary of all relevant observational constraints for the data used in this study.}

In this study, we consider 32 SPLASH fields across the M31 halo ($9 < R_{\text{proj}} < 180$ kpc), sourced from a total of 65 individual slitmasks. Figure 1 shows the position of the slitmasks used with respect to the M31 halo, where the color of the slitmask indicates the known substructure components the field contains (if any).

2.1. Target Selection and Photometry

Targets in our sample were chosen based on their magnitudes and colors. The majority of the sample was selected using imaging taken with the Mosaic Camera on the Kitt Peak National Observatory (KPNO) 4 m Mayall telescope in the Washington system $M$ and $T_2$ filters, and the narrowband DDO51 filter (Ostheimer Jr. 2003; Beaton et al. 2007). Fields in the innermost regions of the halo ($R_{\text{proj}} < 30$ kpc) were designed using imaging obtained in the $g'$ and $i'$ bands using the MegaCam instrument on the CFHT (Gilbert et al. 2012). For subsequent analysis, all magnitudes were transformed into the Johnson system $V, I$ magnitudes, using the relations by Majewski et al. (2000) for imaging obtained in $M$ and $T_2$, and observations of Landolt photometric standard stars for imaging in $g'$ and $i'$. Targets with photometry consistent with being RGB stars at the distance of M31 were assigned a high priority to be included on the spectroscopic slitmasks (Gilbert et al. 2018).

2.2. Spectroscopy and Data Reduction

The spectroscopic slitmasks used in our sample were observed for a nominal total exposure time of 1 hr, with modifications made for particularly good or bad observing conditions. Spectra were obtained with the DEIMOS instrument on the Keck II telescope, using the 1200 line mm$^{-1}$ (1200G) grating, OG550 order blocking filter, which yields a spectral dispersion of 0.33 Å pix$^{-1}$, and resolution of 1.2 Å FWHM. The spectra cover a wavelength range of $\sim6300 \, \text{Å} < \lambda < 9100 \, \text{Å}$, with a resolution of $\sim6000$ at a central wavelength of $\sim7800$ Å. We note that six fields in our sample were also targeted for deep (≤6 hr) observations using the low-resolution ($R \sim 3000$) 600ZD grating (Escala et al. 2020a, 2020b). Science spectra were reduced using the DEEP2 DEIMOS data reduction pipeline, developed by the DEEP2 Galaxy Redshift Survey\footnote{http://deep.ucolick.org/spec2d/} (Cooper et al. 2012; Newman et al. 2013). This software handles flat-fielding, sky subtraction, and extraction of 1D spectra. We applied the modifications described by Simon & Geha (2007) for increased performance with bright stellar sources. Line-of-sight velocities were measured by cross-correlating observed spectra with stellar templates provided by Simon & Geha (2007). Details on the stellar templates used for our sample of RGB stars can be found in Table 2 of Wojno et al. (2020). We used the relative positions of the Fraunhofer A band and other telluric absorption features to correct for the imperfect centering of a star in its slit on the slitmask, following Simon & Geha (2007) and Sohn et al. (2007).

2.3. M31 Membership

We calculated the probability of M31 membership using the velocity model presented by Gilbert et al. (2018). We used the mean of the posterior probabilities of M31 membership for each star, calculated from the M31 and MW likelihoods calculated in the course of the Markov Chain Monte Carlo (MCMC) sampling of the Gaussian mixture model (Section 4.2; Gilbert et al. 2018). The model likelihoods incorporated the prior probability of M31 membership based on the method established by Gilbert et al. (2006) to select stars more likely to be RGB stars at the distance of M31 than foreground MW dwarf stars. This method uses the following photometric/spectroscopic diagnostics: (1) position in $(M - DDO51)$ versus $(M - T_2)$ color–color space, (2) position in $(I, V - I)$ color–magnitude space, (3) equivalent width of the Na I doublet ($\lambda 8183,8195$) as a function of $(V - I)$ color, and (4) comparison between photometric and spectroscopic [Fe/H] measurements. In general, the Gilbert et al. (2006) method also
includes a diagnostic based on the line-of-sight velocity; however, this was not included in calculating the prior probability of M31 membership by Gilbert et al. (2018).

This produces an M31 membership probability \( p_{M31} \) between 0 and 1, where a value of 1 indicates that a star is most likely to belong to M31. We selected M31 members by requiring \( p_{M31} > 0.5 \). For stars with \( R_{\text{proj}} > 90 \text{ kpc} \), we additionally utilized the original M31 membership classification presented by Gilbert et al. (2006), M31CLASS. Based on their likelihood of belonging to M31 using the five diagnostics listed above (including line-of-sight velocity), stars are assigned integer values \( (-3 < \text{M31CLASS} < +3) \), where a value of +3 indicates that the star is very likely to belong to M31. We required M31CLASS = 3 (stars must be three times more likely to belong to M31 than the MW and must not be bluer than the most metal-poor isochrone) for stars with \( R_{\text{proj}} > 90 \text{ kpc} \). This additional criterion was employed for our outermost halo fields because the number of M31 halo stars at these large distances is a small fraction of the observed foreground MW contaminants. We have shown in previous work that with this conservative sample selection, there is no indication of MW contamination in the M31 halo sample at large \( R_{\text{proj}} \) (Gilbert et al. 2012, 2014).

2.4. Substructure Classification

We applied an additional classification to our sample of secure M31 stars to facilitate a comparison between the smooth halo and debris features. The velocity distributions of the most prominent tidal debris features in the SPLASH data have been characterized in previous works (Guhathakurta et al. 2006; Kalirai et al. 2006b; Gilbert et al. 2007, 2009, 2012). The line-of-sight velocity distribution of the M31 halo can be modeled as a Gaussian with a large velocity dispersion (Gilbert et al. 2007), and each substructure component as additional Gaussian components (Gilbert et al. 2007, 2012). These maximum-likelihood fits can then be used to determine the probability that a given star is more likely to belong to the smooth halo or a substructure component.

We adopted substructure probability \( p_{\text{sub}} \) values calculated from previous fits to the velocities of secure M31 stars in individual substructure components as well as the smooth halo, as summarized in Table 4 of Gilbert et al. (2018). For this study, we defined stars with \( p_{\text{sub}} < 0.2 \) as smooth halo stars, and considered all stars with \( p_{\text{sub}} \geq 0.2 \) as potentially associated with substructure. When we examine the histogram of substructure probabilities for our sample, we find a dearth of stars around \( p_{\text{sub}} = 0.2 \), which therefore serves as a dividing line. We note that with this cut, our smooth halo sample may have some contamination from substructure components, and vice versa. This choice minimizes contamination of the smooth halo sample by stars associated with substructure while enabling measurements representing as full a sample of M31’s stellar halo as possible. Applying the division at \( p_{\text{sub}} = 0.2 \) yields 538 smooth halo stars, and 533 stars potentially associated with substructure. While the sample with \( p_{\text{sub}} > 0.2 \) will be dominated by stars potentially associated with substructure, 126 stars, representing 24% of this sample, have \( 0.2 < p_{\text{sub}} < 0.5 \). This means that any abundance differences between the smooth halo and the sample of stars potentially associated with substructure are likely to be underestimated.

After applying the M31 membership criteria (Section 2.4), our sample of all M31 stars consists of 1079 stars across 65 pointings, with 538 belonging to the smooth halo, and 541 that...
have the potential to belong to one of the various substructures in the halo of M31 (Section 5). Figure 2 shows the total number of stars in our sample as a function of their projected distance in kiloparsecs ($R_{\text{proj}}$) from the center of M31, where the top panel shows the distribution of all stars belonging to the smooth halo, as well as those secure abundance measurements. The bottom panel shows the distribution of all stars compared to those likely associated with substructure, as well as those substructure stars that have secure abundance measurements. The projected distance from the center of M31 is calculated using a distance modulus of 24.47 (corresponding to a distance to M31 of 783 kpc; Stanek et al. 1997; McConnachie et al. 2005), in order to facilitate an accurate comparison to literature measurements of the metallicity gradient (Section 6.2).

3. Spectroscopic Abundance Measurements

We used the abundance measurement pipeline presented by Escala et al. (2019) to measure individual [Fe/H] and [$\alpha$/Fe] for all stars in our sample. In summary, the pipeline takes as input a 1D spectrum (and its associated uncertainty array) along with corresponding photometric estimates of $T_{\text{eff}}$, log $g$, and [Fe/H] (Section 3.1), and outputs spectroscopic effective temperature ($T_{\text{eff}}$) along with [Fe/H] and [$\alpha$/Fe]. It compares the observed spectrum to a grid of synthetic spectra (Section 3.2). We allowed $T_{\text{eff}}$, [Fe/H], and [$\alpha$/Fe] to vary iteratively until a best-fit synthetic spectrum is found via $\chi^2$-minimization. The pipeline process for individual spectra is described in Section 3.3. We then built on this methodology to allow the pipeline to handle coadded spectra (Section 3.5; Wojno et al. 2020). Further technical details of the pipeline are described by Escala et al. (2019), and the relevant modifications needed to accommodate for coadded spectra are described by Wojno et al. (2020).

3.1. Photometric Atmospheric Stellar Parameters

We estimated photometric stellar parameters ($T_{\text{eff}}$, log $g$, [Fe/H]$_{\text{phot}}$) by comparing the observed ($V$, $I$) color and $I$ magnitude to a grid of theoretical isochrones. Like Wojno et al. (2020), we adopted the error-weighted mean of the best-fit Padova (Girardi 2016), Victoria-Regina (VandenBerg et al. 2006), and Yonsei-Yale (Demarque et al. 2004) isochrone sets. For these isochrones, we assumed a stellar age of 14 Gyr and [\alpha/Fe] = 0.4 dex for all RGB stars. We shifted the isochrones to the distance of M31 by assuming a distance modulus of 24.63 ± 0.02 (Clementini et al. 2011). We determined photometric $T_{\text{eff}}$, log $g$, and [Fe/H] for each star by linearly interpolating the isochrone grid.

3.2. Synthetic Spectral Grid

In each step of the fitting procedure, the observed spectrum was compared to a grid of synthetic spectra that were generated using the LTE spectral synthesis code MOOG (Sneden 1973), with ATLAS9 stellar atmospheric models (Kurucz 1993; Sbordone et al. 2004; Sbordone 2005; Kirby 2011). The line list was developed using the Vienna Atomic Line Database (Kupka et al. 1999), molecular lines from Kurucz (1992), and a version of the hyperfine transition line list from Kurucz (1993) tuned to match line strengths of the Sun and Arcturus (Kirby 2011; Escala et al. 2020a).

Synthetic spectra were generated for the following parameter ranges: 3500 K < $T_{\text{eff}}$ < 8000 K, 0.0 < log $g$ < 5.0, −5.0 < [Fe/H] < 0.0, and −0.8 < [\alpha/Fe] < +1.2, for a total of 316,848 synthetic spectra (Kirby 2011). The synthetic spectra have a wavelength spacing of 0.02 Å and cover a wavelength range of 6300–9100 Å. When compared to observed spectra, the synthetic spectra were interpolated and smoothed using the observed spectral resolution as a function of wavelength. For individual stars, we assumed that the observed spectral resolution ($\Delta \lambda$ ≈ FWHM/2.35) varies as a function of wavelength, as in Escala et al. (2020a).

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16 We also tested the effect of assuming different distance modulus estimates: 24.47 (McConnachie et al. 2005), and 24.38 (Riess et al. 2012). We found there to be no significant impact on the final measured abundances.
3.3. Chemical Abundance Pipeline

The chemical abundance pipeline used to measure [Fe/H] and \([\alpha/Fe]\) for individual stars is described in detail by Kirby et al. (2008) and Escala et al. (2019), and we summarize here. Modifications made to the chemical abundance pipeline to accommodate coadded spectra are presented by Wojno et al. (2020).

We removed telluric absorption features due to the Earth’s atmosphere using a spectrophotometric standard star (Simon & Geha 2007), where we divided the observed spectra by a scaled template spectrum (Kirby et al. 2015). Observed spectra are shifted to the rest frame according to their line-of-sight velocities. The spectra are then continuum normalized by fitting a third-order B spline to the continuum regions (Kirby et al. 2008), using a breakpoint spacing of 100 pixels.

An initial fit is performed following the initial continuum normalization. In this step, \(T_{\text{eff}}\) and [Fe/H] are allowed to vary simultaneously. While Escala et al. (2019) allowed for the spectral resolution (\(\Delta \lambda\)) to vary as well in this step, we determine \(\Delta \lambda\) as a function of wavelength for each slitmask in our sample, as in Escala et al. (2020a). After fits for \(T_{\text{eff}}\) and [Fe/H] are found, we then allowed \([\alpha/Fe]\) to vary, keeping \(T_{\text{eff}}\) and [Fe/H] constant. The continuum is then re-normalized, using the best-fit synthetic spectrum. This process continues iteratively until the parameter values vary by less than the following tolerance: 1 K in \(T_{\text{eff}}\), 0.001 dex in [Fe/H], and 0.001 dex in \([\alpha/Fe]\). Once the continuum refinement converged, we re-fitted for [Fe/H] and [\(\alpha/Fe\)] and finally [Fe/H] again. Fit uncertainties were calculated as \(\sigma_{\chi^2} = \chi^2_{\text{r}}\), where \(\chi^2_{\text{r}}\) represents the diagonals of the covariance matrix of the fit, and \(\chi^2_{\text{r}}\) is the reduced-\(\chi^2\) statistic for a given fit parameter. We combined this fit uncertainty in quadrature with the systematic uncertainty floors determined in Kirby et al. (2020) of 0.101 dex for [Fe/H], and 0.084 dex for \([\alpha/Fe]\).

We define a star to have secure abundance measurements if all of the following conditions are met: \(\sigma_{\chi^2} < 0.4, \sigma_{[\alpha/Fe]} < 0.4\), the measured value is not at the edge of the grid, and the \(\chi^2\) contours for the [Fe/H] and \([\alpha/Fe]\) fit parameters vary smoothly.

3.4. Removing Stars with TiO

In cool (\(T < 4500\) K) giant stars, TiO absorption can be observed in the optical portion of the spectrum as large sawtooth bands typically in the wavelength range 7055–7245 Å (Jorgensen 1994). This feature is not modeled in our synthetic spectra, and therefore we cannot reliably recover abundances for stars with signatures of TiO absorption. For consistency with previous works in this series using similar data sets, we remove stars with obvious TiO bands from our sample. For stars that pass the quality criteria on their spectroscopic measurements (see Section 3.3), we examine each spectrum for the presence of TiO. Each star is then categorized as having either obvious signatures of TiO, marginal signatures of TiO, or no TiO. For our sample of stars with individual measurements, we find 38% (100), 14% (36), and 48% (125) stars in each category, respectively. For the rest of the analysis, we remove any stars with obvious or marginal signs of TiO.

In Figure 3 we show \((V - I, I)\) color–magnitude space for our categorized stars, color-coded by the detection (or nondetection) of TiO in their spectra. Making a division at \((V - I) = 1.8\) removes the majority of stars with obvious signatures of TiO absorption, with a contamination rate (stars bluer of this cut but still having TiO features in their spectra) of \(\sim 10\%\). For stars without secure individual abundance measurements, which typically have very low S/N, we subsequently consider only those with \(V - I < 1.8\) to remove the majority of stars that are likely to have TiO absorption features in their spectra. This cut preferentially removes cool, metal-rich stars from our sample, and we consider the effects of a bias on the metallicity distribution of our final sample in Section 4.3.

3.5. Coadding Stars

For stars that do not have secure abundance measurements (i.e., they do not pass the quality criteria described in Section 3.3), we combine their spectra to obtain a high enough S/N to obtain an abundance measurement. We identified groups of \(\sim 5\) stars to coadd, with the aim of coadding stars that are as similar as possible in each group.

For stars associated with the smooth halo (\(p_{\text{sub}} < 0.2\), Section 2.4), the sample is first divided into bins according to their projected distance from the center of M31. The boundaries of the radial bins are 10, 15, 19.5, 25, 50, 75, 100, and 125 kpc, as illustrated in Figure 2. For stars that may be associated with substructure (\(p_{\text{sub}} > 0.2\)), the sample is divided by spectroscopic field. For fields with multiple substructure components (e.g., multipeaked velocity distributions), the substructure sample is further divided to ensure that only stars associated with the same velocity component for a given tidal feature are combined. Within each radial bin (smooth halo sample) or field (substructure sample), stars are then sorted according to their photometric [Fe/H] to obtain groups of approximately five stars per coadd.

We then combine the stellar spectra in each photometric [Fe/H] bin according to the coaddition method described by Wojno et al. (2020). First, all spectra are shifted to the rest frame using their observed line-of-sight velocities. The typical line-of-sight velocity uncertainty for stars to be coadded is \(\sim 6.7\) km s\(^{-1}\). The spectra are then continuum normalized, and rebinned such
that the wavelength array of each spectrum covers the wavelength range (6300–9100 Å) with a wavelength spacing of 0.23 Å per pixel to ensure all spectra in the coadd are on the same pixel array. As $\Delta \lambda$ varies for each spectroscopic mask, and stars from different masks can be coadded, we wish to avoid assuming a “coadded” $\Delta \lambda$. The smoothing parameter $\Delta \lambda$ is defined as FWHM/2.35, which for the 1200G grating with a slit width of 0.7 is 0.45. Therefore, for coadded stars, we assume a single fixed value of $\Delta \lambda = 0.45$ (instead of $\Delta \lambda$ varying as a function of wavelength).

The continuum-normalized flux from each spectrum in a given photometric [Fe/H] bin is combined on a pixel-by-pixel basis, weighted by the inverse variance $(1/\sigma^2)$:

$$\tilde{f}_i = \frac{\sum_{j=1}^{n} (f_{\text{pixel},ij} / \sigma^2_{ij})}{\sum_{j=1}^{n} 1 / \sigma^2_{ij}}$$

(1)

where $f_{ij}$ represents the flux of the $i$th pixel of the $j$th spectrum in a group, $\sigma^2_{ij}$ is the variance of $f_{ij}$, and $n$ is the number of spectra to be coadded in a given photometric [Fe/H] bin. The inverse variance weighted flux of the $i$th pixel of the coadded spectra is then given by $\tilde{f}_i$. We also coadd the inverse variance for a group of spectra in a similar way to obtain an inverse variance for the coadded spectrum:

$$\overline{\sigma}_{\text{pixel},i} = \left( \frac{1}{\sum_{j=1}^{n} 1 / \sigma^2_{\text{pixel},ij}} \right)^{-1/2}.$$  

(2)

We then measure [Fe/H] and $[\alpha/Fe]$ following the spectroscopic synthesis and fitting procedure described by Wojno et al. (2020). The method for coadded spectra is similar to that for individual spectra, with the following modifications: (1) we assume a fixed value for $\Delta \lambda$, and (2) the coadded spectrum is compared to synthetic spectra that have been coadded using the same inverse variance arrays as the observed spectra.

For each coadded spectrum, we checked the $\chi^2$ fit contours for [Fe/H] and $[\alpha/Fe]$ to confirm that the minimum is well defined. If the fit contours were not well defined, we removed stars with low S/N from the coadd and reassessed the coadded spectrum until we achieved a good fit. We also propagated uncertainties arising from uncertainties in the photometric measurements of $T_{\text{eff}}$ and log $g$ (Wojno et al. 2020). The fit uncertainty and photometric uncertainty were added in quadrature to the systematic uncertainty floors of 0.101 dex for [Fe/H], and 0.084 dex for $[\alpha/Fe]$ (Kirby et al. 2020).

4. Spectroscopic Abundance Gradients in the M31 Halo

We analyze trends in [Fe/H] and $[\alpha/Fe]$ as a function of $R_{\text{proj}}$ for the smooth halo of M31, as well as stars possibly associated with tidal debris features. Our smooth halo sample consists of 91 individual stars with [Fe/H] and $[\alpha/Fe]$ measurements satisfying the quality criteria (see Section 3.3) and 64 coadds, the latter representing an additional 272 stars. Our sample of stars potentially associated with substructure consists of 69 stars with [Fe/H] and $[\alpha/Fe]$ measurements, and 53 coadds representing an additional 271 stars. In Section 4.1, we explore gradients in [Fe/H] as a function of projected radius, for the smooth halo as well as stars associated with substructure. We explore gradients in $[\alpha/Fe]$ as a function of projected radius in Section 4.2. We identify and attempt to address potential sources of bias in measurements of the [Fe/H] gradient arising from the presence of TiO absorption in our spectra in Section 4.3. Finally, we look at the [Fe/H]–$[\alpha/Fe]$ distribution as a function of projected radius for the smooth halo in Section 4.4. The [Fe/H] and $[\alpha/Fe]$ distributions for individual fields containing known substructure(s) are presented in Section 5.

4.1. [Fe/H] Metallicity Gradients

The halo of M31 is known to have a significant radial metallicity gradient (Kalirai et al. 2006a; Koch et al. 2008; Gilbert et al. 2014; Escala et al. 2020a). To measure the spectroscopic metallicity gradient, we assume it follows a linear model parameterized by an angle $\theta$, the perpendicular distance of the line from the origin $b_\perp$, and some intrinsic scatter $V$. The intrinsic scatter parameter allows us to make the assumption that the uncertainties on our measurements are underestimated, or there is some intrinsic scatter present in our data. Intrinsic scatter in the abundances is expected, as stellar halos encode a complex history of star formation and accretion that differs from location to location. We prefer this parameterization over the standard $(m, b)$ because it avoids the preference for shallow slopes when flat priors are used (Hogg et al. 2010). Uncertainties on both [Fe/H] and $[\alpha/Fe]$ are taken into account when comparing our measured abundances to the model, and we assume flat priors on $\theta$, $b_\perp$, and $V$.

To find the best-fit parameters, we maximize the likelihood:

$$\ln L = K - \sum_{i=1}^{N} \frac{1}{2} \ln(\Sigma_i^2 + V) - \sum_{i=1}^{N} \frac{\Delta_i^2}{2(\Sigma_i^2 + V)}$$

(3)

where $\Sigma_i^2$ represents the uncertainty for each data point, $\Delta_i^2$ is the orthogonal displacement of each data point from the line model, and $K$ is a constant (Hogg et al. 2010). We maximize this likelihood using emcee, a python implementation of an MCMC Ensemble sampler (Foreman-Mackey et al. 2013), following the same method described by Wojno et al. (2020). With emcee, we generate a distribution of linear models that fit our data, taking the 50th percentile of the marginalized posterior distribution as our measured gradient, and the average of the 16th and 84th percentiles as the quoted uncertainty on the gradient. The measured gradients for all subsamples described in this section are given in Table 1.

4.1.1. Smooth Halo Stars

Figure 4 shows [Fe/H] as a function of projected radius from the center of M31 for our sample of smooth halo stars with either individual or coadded spectroscopic [Fe/H] and $[\alpha/Fe]$ abundances. For the individual and coadded measurements, which cover a radial range $R_{\text{proj}}$ of 8–177 kpc, we measure a slope of $-0.0075 \pm 0.0012$ dex kpc$^{-1}$, indicated by the solid magenta line the top-left panel in Figure 4. We also show the metallicity gradient fit using only stars with individual [Fe/H] measurements (black line), where we measure a value of $-0.0053 \pm 0.0012$.

Considering the difference in the distributions between the individual and coadded measurements, the spectra that are coadded typically have low S/N, and/or are more metal-poor and therefore have weaker lines. Therefore, it is reasonable that the metallicity gradient measured from individual stars is shallower because it leaves out a significant number of metal-poor ([Fe/H] $<-1.5$ dex) stars at more distant projected radii.
Note. The number in parentheses in the $N_{\text{coadds}}$ column refers to the number of stars that went into the coadds.

(R$_{\text{proj}} > 50$ kpc). We consider the combined individual and coadded abundances to be the most comprehensive sample for measuring the radial metallicity gradient of the smooth halo.

For comparison, we also show the photometric [Fe/H] for secure M31 smooth halo stars (gray points) in addition to the slope measured by Gilbert et al. (2014) using photometric [Fe/H] for a sample of secure M31 smooth halo stars out to a projected radius of 90 kpc. We note that the sample used to determine the photometric [Fe/H] gradient includes stars with signs of TiO absorption, and used different criteria to define stars more likely associated with the smooth halo than substructure components. We find that the slope of the gradient measured using both the individual and coadded abundance measurements agrees within 2σ with the value of the gradient measured from photometric [Fe/H], albeit with an offset on the normalization. If we restrict our sample of individual and coadded measurements to the same radial range as the Gilbert et al. (2014) measurements ($R_{\text{proj}} < 90$ kpc), the gradient is unchanged.

In the bottom-left panel of Figure 4, we show the inner 35 kpc of our smooth halo sample. In addition to our sample (black points), we show the spectroscopic [Fe/H] abundances from Escala et al. (2020b), where they used deep (∼6 hr, 600ZD grating) observations of fields in the inner halo of M31 to obtain spectroscopic abundances for a sample of individual stars significantly overlapping our own (six in common out of 10 spectroscopic fields in our sample with $R_{\text{proj}} < 35$ kpc). Escala et al. (2020b) found a radial [Fe/H] gradient of $-0.025 \pm 0.002$ dex kpc$^{-1}$, shown in the bottom-left panel of Figure 4 as a dashed blue line. To facilitate a more accurate comparison to the measurements from Escala et al. (2020b), we remeasure the radial [Fe/H] gradient using all individual and coadded smooth halo measurements within $R_{\text{proj}} < 35$ kpc, finding a value of $-0.018 \pm 0.003$ dex kpc$^{-1}$ (dashed magenta line), consistent within $\sim 2\sigma$.

4.1.2. Substructure

The right-side panels of Figure 4 show stars potentially associated with substructure (blue), where individual abundance measurements are indicated with filled points, and coadds are open circles. For individual and coadded [Fe/H] measurements, we measure a gradient of $-0.0086 \pm 0.0023$ dex kpc$^{-1}$, indicated with a solid cyan line. This gradient is fit to a smaller radial extent compared to the smooth halo, as the most distant substructure identified in SPLASH is at ∼90 kpc. We also measure a gradient of $-0.0084 \pm 0.0008$ dex kpc$^{-1}$ for the combined sample of all M31 stars (both the smooth halo and substructure samples), using both individual and coadded measurements.

In the bottom-right panel of Figure 4, we show our sample limited to a radial range of $R_{\text{proj}} < 90$ kpc. The solid blue line is the same fit from the top-right panel, for individual and coadded stars in both the smooth halo and substructure samples. We also fit this gradient using a restricted radial range ($R_{\text{proj}} < 90$), finding a value of $-0.0078 \pm 0.0020$ (dashed blue line), for comparison to the gradient measured using both smooth halo and substructure from Gilbert et al. (2014; purple dotted line). Compared to the gradient measured by Gilbert et al. (2014), we find that our measured gradient for all stars in this restricted radial range is consistent within $\sim 2\sigma$, with an offset of approximately 0.5 dex with respect to the normalization.

4.2. [$\alpha$/Fe] Abundance Gradients

In Figure 5, we show [$\alpha$/Fe] as a function of projected radius, for the smooth halo sample (black points) as well as the sample of stars possibly associated with substructure (blue points). Using individual (filled points) and coadded measurements (open points) for smooth halo stars, we find a best-fit gradient of $+0.0030 \pm 0.0009$ dex kpc$^{-1}$, shown as a solid magenta line, with the shaded regions indicating 1σ uncertainties. This is consistent with the gradient measured from individual [$\alpha$/Fe] measurements only (black line, $+0.0031 \pm 0.0010$ dex kpc$^{-1}$). When we consider only stars possibly associated with substructure in the top-right panel of Figure 5, we measure a value of $+0.0020 \pm 0.0030$ dex kpc$^{-1}$, consistent with no gradient (cyan line). For the full sample of individual and coadded measurements for all stars (smooth halo and substructure samples), we measure a gradient of $+0.0027 \pm 0.0005$ dex kpc$^{-1}$ (blue line).

The bottom-left panel of Figure 5 is analogous to the bottom-left panel of Figure 4, where we compare our sample to the sample presented in Escala et al. (2020b; light-blue points). Escala et al. (2020b) measured an [$\alpha$/Fe] gradient of $+0.0029 \pm 0.0027$ dex kpc$^{-1}$ for smooth halo stars 8–35 kpc in projected radius, shown as the dashed light-blue line. This value is consistent with our value for the smooth halo using both individual and coadded abundance measurements ($+0.0030 \pm 0.0009$). If we restrict our smooth halo sample to the same radial range as the Escala et al. (2020b) sample (8–35 kpc), we measure a slightly steeper gradient of $+0.0055 \pm 0.0020$ dex kpc$^{-1}$ (dashed magenta line). In the bottom-right plot, we compare the gradient measured for all individual stars and coadds (solid blue line) and the gradient from Escala et al. (2020b) to the gradient measured using all stars within 35 kpc ($+0.0030 \pm 0.0017$ dex kpc$^{-1}$ dex kpc, dashed blue line). The measured gradient for all stars in this restricted radial range falls between the Escala et al. (2020b) measurement and the gradient found for our full sample (all stars, including individual and coadded measurements), and is consistent within 2σ with the latter.
Figure 4. Spectroscopic [Fe/H] vs. projected radius for stars with individual/coadded (filled/open circles) [Fe/H] measurements. Gray points are photometric [Fe/H] measurements for our sample. Top left: the best-fit spectroscopic [Fe/H] gradient for individual smooth halo stars (Section 4.1.1, solid black), where the shaded regions indicate a 1σ standard deviation. The red dotted line represents the gradient measured by Gilbert et al. (2014) for smooth halo stars, using photometric [Fe/H]. The magenta line shows the best-fit gradient calculated using both individual stars and coadds (Section 3.5). Bottom left: [Fe/H] measurements for a limited radial range (R$_{proj}$ < 35 kpc). The sample of Escala et al. (2020b) is shown as light-blue points, and the gradient measured with their sample is shown as a dashed blue line. The solid magenta line is the same as the top-left panel. We also show the fit after limiting our sample to the same radial range (dashed magenta). Top right: individual/coadded (filled/open dark blue squares) [Fe/H] measurements for stars potentially associated with substructure (Section 2.4), with the best-fit gradient to individual and coadded measurements from the substructure sample (cyan), and the gradient including all stars (both the smooth halo and substructure samples; blue). The photometric [Fe/H] gradient from Gilbert et al. (2014), fit using smooth halo and substructure stars, is shown as a dashed purple line. Bottom right: the same as above, but for a limited range (R$_{proj}$ < 90 kpc). Regardless of our sample selection, we recover a statistically significant metallicity gradient in the halo of M31.

There are multiple potential sources for the differences between our measured gradients and those measured by Escala et al. (2020b). Measuring reliable [$\alpha$/Fe] abundances with shallow 1200G spectra is typically more difficult compared to the deep 600ZD spectra used in the Escala et al. (2020b) sample, due to both the higher S/N of the deep 600ZD spectra, and the expanded spectral range toward the blue (4100–9000 Å), which provides significantly more lines for measuring $\alpha$-elements. Our sample has a larger number of stars with [$\alpha$/Fe] ~ −0.5 at small projected radii (R$_{proj}$ < 25 kpc), which may serve to "tilt" the gradient toward the positive direction. In addition, as the coadd technique increases the ability to recover abundance measurements for metal-poor stars, and there is a general relationship between [$\alpha$/Fe] and [Fe/H], the addition of measurements from coadded spectra will tend to add more $\alpha$-enhanced stars to the sample of abundance measurements. This may also result in a more positive measured gradient, as the fraction of metal-poor stars is higher at larger projected radius. In summary, while evidence for a gradient in [$\alpha$/Fe] as a function of R$_{proj}$ for the inner regions of the M31 halo is tentative at best, we find that there is a significant radial gradient in [$\alpha$/Fe] over the entire radial range that we consider for this study.

4.3. Effect of Excluding Stars with TiO

We have removed stars likely to have TiO absorption from our spectral synthesis abundance measurements (Section 3.4), as the synthetic spectra used in our spectroscopic abundance pipeline do not model TiO absorption, and therefore we cannot reliably measure abundances for stars with significant TiO absorption features. Our secure M31 sample contains 1079 stars, and we remove 308 stars (~29%) that are either observed or are likely to have TiO absorption features. The removal of stars with TiO absorption features removes predominantly cool, metal-rich stars. As these TiO stars make up a significant portion of our M31 halo sample, in this section we attempt to quantify any potential bias on the radial metallicity gradient measurement due to the removal of these stars.

To do this, we use the photometric metallicities of all smooth halo stars (including those with likely TiO absorption) to find...
the average $[\text{Fe/H}]_{\text{phot}}$ for a given radial bin, and compare this to the average $[\text{Fe/H}]_{\text{phot}}$ of the radial bin after we remove stars with TiO. We define a TiO correction factor, $[\text{Fe/H}]_{\text{TiO corr}}$, as the difference in the mean $[\text{Fe/H}]_{\text{phot}}$ between the two averages for each radial bin.

In Figure 6, we show the estimated bias in our $[\text{Fe/H}]$ gradient measurement due to removing stars likely to have TiO in their spectra. The top panel shows photometric $[\text{Fe/H}]$ as a function of projected radius for secure M31 smooth halo stars, with smooth halo stars that do not pass our TiO cuts shown in yellow. The overplotted diamonds represent the weighted mean photometric metallicity for a given radial bin, for all smooth halo stars (yellow) and for stars unlikely to have TiO in their spectra following the criteria in Section 3.4 (dark purple). The mean $R_{\text{proj}}$ is calculated using the position of all points in a given radial bin. The TiO correction factor, $[\text{Fe/H}]_{\text{TiO corr}}$, is defined as the difference between these means, and is of the order of $\sim0.1$ dex for any given radial bin. This correction factor estimates the shift of the mean metallicity if we were to include stars with TiO absorption in their spectra.

The solid magenta line shows the spectroscopic $[\text{Fe/H}]$ gradient measured using both the individual and coadded abundance measurements for the smooth halo sample (Section 4.1.1). The red dotted line is the gradient presented in Gilbert et al. (2014), measured using photometric metallicities of stars in the smooth halo of M31 (see their Figure 10). We include this measurement for comparison as their sample selection is similar to our sample selection (including TiO stars; Section 2.3), although the gradient is fit over a smaller radial range ($R_{\text{proj}} < 90$ kpc). Their measured gradient ($-0.0105 \pm 0.0013$ dex kpc$^{-1}$) is consistent (within $2\sigma$) with what we measure from both individual and coadded spectroscopic measurements of stars in the smooth halo, with a vertical offset of approximately 0.5 dex.

In the bottom panel of Figure 6, we show the sample of individual smooth halo stars with spectroscopic $[\text{Fe/H}]$ measurements (filled points) and coadded $[\text{Fe/H}]$ measurements (open points). The mean spectroscopic $[\text{Fe/H}]$ for each radial bin is indicated with dark purple diamonds. The yellow diamonds represent the weighted mean $[\text{Fe/H}]$ plus $[\text{Fe/H}]_{\text{TiO corr}}$ for a given radial bin. We remeasure the radial gradient using only these mean measurements, resulting in the “uncorrected” (dark purple) and “corrected” (yellow) fits indicated with dashed lines. The shaded regions indicate $1\sigma$ uncertainties. The slope of the gradient that we measure from the “corrected” measurements is consistent ($-0.0079 \pm 0.0020$) with the gradient measured from the “uncorrected” means ($-0.0072 \pm 0.0021$), and is encapsulated within the

![Figure 5](image_url)
large uncertainties of the fits. We estimate that the effect on the radial metallicity gradient due to removing TiO stars from our sample produces an offset on the normalization of approximately the order of the TiO correction factor (~0.1 dex), and does not significantly affect the measured slope. Since there is significant dispersion in the [α/Fe] values as a function of [Fe/H] (Section 4.4), we cannot reasonably estimate the potential bias on the [α/Fe] gradient due to removing stars with TiO.

4.4. [Fe/H]–[α/Fe] Distribution as a Function of Radius

We combine both the [Fe/H] and [α/Fe] spectroscopic abundance information in Figure 7, where we show the [Fe/H]–[α/Fe] distribution as a function of radius for our nine radial bins. We show both the individual (black points) and coadded (open circles) abundance measurements for smooth halo stars. For comparison, we also show the spectroscopic sample from Escala et al. (2020b; blue points).

The mean [Fe/H] shifts as a function of projected radius, from primarily metal-rich populations in the inner regions, to relatively metal-poor populations in the most distant regions of the smooth halo. Given the aspect ratio of the plots, the [α/Fe] abundance gradient is more difficult to detect in the 2D abundance space by eye; however, there are distinct differences if we compare the more centrally concentrated bins (R_{proj} < 20 kpc) to the outermost bins.

We find that both our individual and coadded abundance measurements follow the abundance distribution of the Escala et al. (2020b) sample, for the regions where our samples overlap. The spread of the distribution varies significantly for each radial bin. The outermost bins (R_{proj} > 50 kpc) have slightly smaller dispersions in [Fe/H] and [α/Fe], but these bins are more susceptible to small number statistics, and therefore we do not detect any correlation between dispersion in [Fe/H] or [α/Fe] with increasing projected distance. For bins larger than 50 kpc, we present some of the first spectroscopic abundance measurements for stars at large projected radii. Prior to this work, only nine stars in M31’s outer halo (43 < R_{proj} < 165 kpc) had spectroscopic [Fe/H] and [α/Fe] measurements (Vargas et al. 2014; Gilbert et al. 2020). We measure spectroscopic [Fe/H] and [α/Fe] abundances for 45 halo stars with R_{proj} > 50 kpc, providing an increase of 600% in outer halo stars with [α/Fe] and [Fe/H] measurements. In addition, we have 33 coadded measurements of outer halo stars, representing the averaged abundances of an additional 174 individual stars.

5. Substructure

In this section we explore the chemical abundances of stars that may belong to various substructures in M31’s halo. The analysis was done on a field-by-field basis, where multiple masks/poinings were merged for the final sample for that field (e.g., Gilbert et al. 2012). To obtain coadded measurements for stars likely associated with substructure, they are first grouped by their observed field. For example, a0_1, a0_2, and a0_3 are three masks observed in the same GSS field, and thus we consider candidates for coaddition from those three masks combined. As for the smooth halo sample, we sort stars according to their photometric [Fe/H] to obtain groupings of approximately five stars per coadd. For fields that contain multiple substructures/debris features, we coadd stars according to their line-of-sight velocity measurements as well as photometric [Fe/H] (see Figures 9–12).

As discussed in Section 2.4, we intentionally chose a division between smooth halo and substructure samples (ρ_{sub} = 0.2) that minimizes contamination by substructure in the smooth halo sample. While it is not possible to isolate a pure substructure sample from line-of-sight velocities alone, the choice of ρ_{sub} > 0.2 for the substructure sample does increase the fraction of stars associated with the smooth halo included in the substructure sample compared to using a higher ρ_{sub} value. It has been shown in previous works (Escala et al. 2020b) that the abundance distributions of the smooth halo and substructure components overlap considerably in M31’s inner halo. The inclusion of a higher fraction of smooth halo stars in the substructure sample will tend to increase the apparent overlap in chemical space, and thus the true differences between smooth halo and substructure can be expected to be larger than seen here.

In this work, our fields target or overlap the following named substructures in the halo of M31: the GSS (Ibata et al. 2001), a Kinematically Cold Component (KCC) associated with the GSS (Gilbert et al. 2009, 2019), Stream C (Ibata et al. 2007),

![Figure 6](image-url)
and the Southeast Shelf (Gilbert et al. 2007). We also only have coadded measurements for fields f135 and A220, located at 17 and 85 kpc in $R_{\text{proj}}$, respectively. These fields have previously been identified as having substructure (Gilbert et al. 2012); however, they are not associated with the named substructures listed above. The locations of these fields with substructure are shown in Figure 1, overplotted on the stellar density map of M31 from PAndAS (McConnachie et al. 2018) to illustrate the position and extent of the relevant substructure(s).

5.1. $[\alpha/\text{Fe}]-[\text{Fe/H}]$ Distribution as a Function of Radius

In Figure 8, we show the distribution of stars in $[\text{Fe/H}]-[\alpha/\text{Fe}]$ space for both our smooth halo and substructure samples. We also show coadded abundance measurements for both the smooth halo and each of the substructure components in our sample. The substructure coadds are color-coded according to the substructure with which they are associated. We use the same colors for each substructure/field for the rest of this section.

In a number of radial bins, we find that the distributions of stars possibly associated with substructure components vary similarly as compared to the distribution of smooth halo stars, in the sense that stars at small $R_{\text{proj}}$ are on average more metal-rich than stars at large $R_{\text{proj}}$. In addition, we find that stars potentially associated with any substructure in the M31 halo are on average more metal-rich (higher $[\text{Fe/H}]$), and have lower $[\alpha/\text{Fe}]$ (Figures 9–12), compared to the smooth halo stars in the same radial bin. However, overall the substructure components also tend to follow the same radial $[\text{Fe/H}]$ gradient as the smooth halo. Indeed, we measure nearly the same halo $[\text{Fe/H}]$ gradient if we include all substructure, compared to the $[\text{Fe/H}]$ gradient measured for the smooth halo only. Some of these substructures (GSS, SE shelf) likely originate from the same merger event (Escala et al. 2021), and we find that qualitatively, the distributions of these two components are more similar to each other than the underlying M31 smooth halo. In the following sections, we explore the abundance distributions for each of the substructure components separately.

Figure 7. $[\alpha/\text{Fe}]-[\text{Fe/H}]$ as a function of projected radius for our nine radial bins. The corresponding radial range for a given panel is indicated in the bottom left. In each panel, we show the sample of smooth halo stars with individual abundance measurements (black points), coadded smooth halo stars (open circles), and the sample from Escala et al. (2020b; blue points). The mean $[\text{Fe/H}]$ and $[\alpha/\text{Fe}]$ for each radial bin for our sample including both individual and coadded measurements are shown as solid gray lines. We find that the mean $[\text{Fe/H}]$ gradually shifts to lower metallicities as a function of increasing projected radius, and that outermost radial bins have a higher mean $[\alpha/\text{Fe}]$ compared to the inner bins.
5.2. Giant Stellar Stream

The GSS is immediately identifiable in stellar density maps of the halo of M31 (Ibata et al. 2001) as a radial structure extending approximately 6° (~80 kpc) to the south of M31’s center, to the west of the southern minor axis. The core of the GSS is metal-rich and has a high surface brightness, while photometric studies have shown the envelope is relatively more metal-poor and has a lower surface brightness (Ibata et al. 2001; McConnachie et al. 2003, 2018). The stellar density sharply declines along the eastern edge of the GSS, and decreases gradually across the western envelope.

Our observations target fields on the core (a3, f207, H13s; Section 5.2.1) as well as the envelope of the GSS (a13; Section 5.2.2). The mean velocity of stream members varies as a function of projected radius, from $-524.9 \text{ km s}^{-1}$ at 17 kpc to $-301.6 \text{ km s}^{-1}$ at 58 kpc, and for this work we adopt the values for each kinematic component as a function of radius compiled in Table 4 of Gilbert et al. (2018).

5.2.1. GSS Core

In Figure 9, we show the (a) line-of-sight velocity histogram, (b) spectroscopic $[\text{Fe/H}]$ histogram, (c) line-of-sight velocity versus $[\text{Fe/H}]$, and (d) $[\text{Fe/H}]$ versus $[\alpha/\text{Fe}]$ for stars likely belonging to substructure (outlined points), and those belonging to our M31 smooth halo sample (gray). Field f207 is 17 kpc in projected radius from the center of M31. Gilbert et al. (2019) provides a thorough overview of this field, where they use deeper spectroscopic observations to investigate the three kinematical components in the field: the GSS, a KCC, and a kinematically hot halo component. Field H13s is located at 21 kpc from the center of M31, roughly southeast along the minor axis, and spatially overlaps with the deeper spectroscopic observations of field S, presented in Escala et al. (2020a). This field contains substructure associated with both the GSS and KCC. Field a3 is located at 33 kpc in projected radius, and is the most distant field along the core of the GSS. Deep (~6 hr) spectroscopic observations of this field were published in
as well as coadded groupings of stars and velocity dispersion. The systemic velocity with substructure in spectroscopic (mean to the smooth halo of M31 in the same radial range. We measure a

Escala et al. 2020b, and the substructure component was subsequently analyzed in Escala et al. 2021. For these three fields, we obtain abundance measurements for 15 individual stars, and 27 coadds, representing an additional 136 stars.

We find that the [Fe/H]–[α/Fe] distribution of the substructure sample from both individual and coadded spectroscopic measurements (Figure 9) is similar, but slightly more metal-rich, compared to the smooth halo of M31 in the same radial range. We measure a mean [Fe/H] of $-1.080 \pm 0.005$ ($\sigma_{\text{Fe/H}} = 0.49$) and a mean $[\alpha/\text{Fe}]$ of $0.340 \pm 0.012$ ($\sigma_{[\alpha/\text{Fe}]} = 0.39$) for the smooth halo in the radial range spanned by these fields ($10 < R_{\text{proj}} < 50$ kpc). For all individual and coadded stars potentially associated with the GSS, we find a mean [Fe/H] of $-0.859 \pm 0.004$ ($\sigma_{\text{Fe/H}} = 0.35$) and a mean $[\alpha/\text{Fe}]$ of $0.107 \pm 0.017$ ($\sigma_{[\alpha/\text{Fe}]} = 0.43$).

This value differs slightly from the mean [Fe/H] reported in Escala et al. (2021) of $-1.03 \pm 0.07$, where they used a sample of stars that overlaps the sample presented in this work, using deeper (~6 hr) observations made with the 600ZD grating on DEIMOS. This grating allows for expanded wavelength coverage at the blue end at the expense of lower resolution. Additional validation of the agreement between stars observed with 600ZD and 1200G grating has been presented in Wojno et al. (2020) and Escala et al. (2020a). However, we note that Escala et al. (2021) applies a different criterion to obtain their sample of stars likely associated with substructure ($p_{\text{sub}} > 0.5$), while our sample of stars possibly associated with substructure is more likely to be contaminated by smooth halo stars ($p_{\text{sub}} \geq 0.2$).

5.2.2. GSS Envelope

Field a13 is located at approximately 58 kpc in projected distance from the center of M31, on the western side of the envelope of the GSS. Photometric studies have found the envelope to have a lower surface brightness and metallicity compared to the GSS core (Ibata et al. 2007). Using SPLASH data to identify GSS stars, Gilbert et al. (2009) found a photometric metallicity difference between the GSS core (fields f207, H13s, and a3) and envelope (a13) of ~0.7 dex. Escala et al. (2021) used an overlapping sample of M31 RGB stars observed with the 600ZD grating on DEIMOS to explore abundance gradients in the GSS. They measure a difference in the spectroscopic [Fe/H] of ~0.1 dex between the core and envelope of the GSS. For field a13, we obtain abundance measurements for five individual stars, and three coadds representing an additional 15 stars.

Figure 10 shows stars in a13 possibly associated with substructure (light-green) compared to the smooth halo sample from the same radial bin as field a13 (gray; $50 < R_{\text{proj}} < 75$ kpc). We find that stars in the GSS envelope and smooth halo samples
have a similar mean [Fe/H] but the mean [α/Fe] of the GSS envelope sample is significantly lower (−0.6 dex). For the GSS envelope sample, we measure a mean [Fe/H] of −1.459 ± 0.011, (σ[Fe/H] = 0.39), and a mean [α/Fe] of 0.066 ± 0.026 (σ[Fe/H] = 0.36). In comparison, for the smooth halo sample in the same radial range, we measure a mean [Fe/H] of −1.391 ± 0.013, (σ[Fe/H] = 0.39), and a mean [α/Fe] of 0.670 ± 0.032 (σ[Fe/H] = 0.34). The mean [α/Fe] (0.066 ± 0.026) for this field agrees more closely with the GSS core fields (0.107 ± 0.017), despite a difference of approximately 40 kpc in projected radius. We note that the ⟨[α/Fe]⟩ that we measure for the GSS core and the GSS envelope samples are significantly lower compared to the values presented in Escala et al. (2021), using deep 600ZD observations of a similar set of fields. This may be due, at least in part, to the differing $p_{sub}$ thresholds used in the two analyses.

5.3. Stream C

Field m4 is located on the minor axis of M31. This field is known to contain multiple kinematical components, and spatially overlaps “Stream C,” a debris stream perpendicular to the GSS. This stream was first detected using deep photometric data (Ibata et al. 2007), and was targeted for spectroscopic follow-up (Chapman et al. 2008). Chapman et al. (2008) found that the stream is composed of two distinct kinematic structures that overlap spatially: a primary metal-rich ([Fe/H] ∼ −0.6 dex) component with a systemic velocity of −349 km s$^{-1}$, and a secondary metal-poor ([Fe/H] ∼ −1.3 dex) component with a systemic velocity of −286 km s$^{-1}$. Both components were determined to have similar velocity dispersion, $σ_v$ 5 km s$^{-1}$. These properties were confirmed by Gilbert et al. (2009) using the m4 field, located at a slightly different location on Stream C than the Chapman et al. (2008) spectroscopic sample.

Our sample of stars in m4 has a mean projected radius of 58 kpc. We obtain abundance measurements for 11 individual stars, and five coadds, representing an additional 26 stars. Figure 11 shows the line-of-sight velocity histogram, metallicity ([Fe/H]) histogram, [Fe/H] versus line-of-sight velocity distribution, and [Fe/H]−[α/Fe] distribution for stars possibly associated with substructure in m4, as well as stars in the smooth halo sample in the same radial bin as field m4 (50 < R$_{proj}$ < 75 kpc). Stars in this field have a bimodal velocity distribution, with peaks around −350 and −250 km s$^{-1}$ (Gilbert et al. 2018). The individual spectroscopic metallicities of stars potentially associated with the two kinematically cold components follow the same pattern found in earlier work: the more negative peak at −354.8 km s$^{-1}$ is on average more metal-rich than the peak at −254.1 km s$^{-1}$. In this work, we measure a mean [Fe/H] of −1.18 ± 0.02 for stars associated with the more negative peak in the velocity distribution, and a mean [Fe/H] of −1.49 ± 0.03 for stars associated with the peak at −254.1 km s$^{-1}$. Compared to the smooth halo, we find that the stars possibly associated with stream C are slightly more metal-rich ([Fe/H] = −1.313 ± 0.007, σ[Fe/H] = 0.36) compared to the smooth halo ([Fe/H] = −1.599 ± 0.007, σ[Fe/H] = 0.36), and have a lower mean [α/Fe] (0.199 ± 0.020, σ[α/Fe] = 0.38)
compared to the smooth halo ($\langle \alpha/Fe \rangle = 0.394 \pm 0.018, \sigma(\alpha/Fe) = 0.34$).

### 5.4. Southeast Shelf

The southeast shelf substructure was first presented in Gilbert et al. (2007), where they describe it as a kinematically distinct cold component of the velocity distribution. Using photometrically derived metallicity estimates, they find that the stars likely to belong to this substructure are more metal-rich than smooth halo stars at the same radial range. The presence of this shelf feature has been predicted by N-body models for the GSS progenitor (Fardal et al. 2007), where the SE shelf is a shell formed by the fourth pericentric passage of tidal debris from the GSS progenitor (Fardal et al. 2006, 2007).

Escala et al. (2020a), using deep 600ZD spectroscopic observations of M31 inner halo stars ($R_{\text{proj}} \sim 12$ kpc), compared the abundances of stars associated with the GSS to those in the SE shelf. They found that the SE shelf was $\geq 0.1$ dex more metal-poor than the GSS at the same range of projected radii. They indicate that this may be evidence for the presence of a radial metallicity gradient in the GSS progenitor, if the GSS and SE shelf are indeed related. Escala et al. (2021) added another field to this analysis, at a larger distance in projected radius ($R_{\text{proj}} \sim 18$ kpc) to be able to reliably disentangle the substructure component from the background halo population via line-of-sight velocity. With deep 600ZD and 1200G spectroscopy, they compared the spectroscopic metallicity and abundance distributions between the GSS and the SE shelf with this expanded sample, finding that the mean measured abundances agree within $1\sigma$. They find that both distributions are consistent with being drawn from the same distribution, further indicating they originate from the same merger event.

Our sample of stars possibly associated with this substructure is drawn from fields f115, f116, and f123. These fields are located at 13, 15, and 17 kpc, respectively, in projected distance from the center of M31. We obtain abundance measurements for 21 individual stars and 14 coadds, representing an additional 72 stars. In Figure 12, we show the comparison between our SE shelf sample (blue symbols), and the smooth halo sample in the same radial range as the SE shelf fields (10 $< R_{\text{proj}} <$ 19.5 kpc, gray). We find that stars that are potentially associated with the SE shelf substructure have a very similar mean $[\text{Fe/H}]$ ($-0.93 \pm 0.01, \sigma(\text{Fe/H}) = 0.41$) compared to the smooth halo ($\langle \text{Fe/H} \rangle = -0.94 \pm 0.01, \sigma(\text{Fe/H}) = 0.49$). In addition, we measure a mean $[\alpha/\text{Fe}]$ for our SE shelf sample of $0.06 \pm 0.02 \sigma(\alpha/\text{Fe}) = 0.46$, which is lower than the mean $[\alpha/\text{Fe}]$ for the smooth halo ($\langle \alpha/\text{Fe} \rangle = 0.36 \pm 0.02, \sigma(\alpha/\text{Fe}) = 0.42$). Compared to the GSS core and envelope fields, the SE shelf has a mean $[\text{Fe/H}]$ more similar to the GSS core, but the mean $[\alpha/\text{Fe}]$ is consistent within $2\sigma$ to both the GSS core and GSS envelope fields.

### 6. Discussion

In this work, we find abundance gradients in both $[\text{Fe/H}]$ and $[\alpha/\text{Fe}]$ as a function of projected radius from the center of M31. These gradients are measured using spectroscopic abundance measurements for individual M31 RGB stars with high-quality spectra, as well as coadded abundance measurements for groups of low-S/N stars. In addition, we also explore
the $[\text{Fe/H}]$–$[\alpha/\text{Fe}]$ abundance distribution as a function of projected radius, for both the smooth halo, as well as multiple tidal debris components present in the M31 halo sample.

6.1. The Outer Halo of M31

It is well established that halos of massive galaxies form primarily through hierarchical accretion, i.e., are built up through the tidal disruption of less-massive satellite galaxies (e.g., Searle & Zinn 1978; Bullock & Johnston 2005; Font et al. 2011; Conroy et al. 2019). In the halo of M31, the GSS provides the most significant evidence of a recent/ongoing accretion event, where the satellite debris is not yet phase mixed, and is therefore visible as streams and shells (Ibata et al. 2001; Ferguson et al. 2002; Fardal et al. 2007, 2008). However, a significant population of stars in the outer halo of M31 are not associated with known substructure, which in this work we call the “smooth halo.” Of particular interest are the smooth halo stars found at large projected radii from the center of M31 ($R_{\text{proj}} > 50$ kpc). In this section, we will attempt to provide constraints on the origin of these outer smooth halo stars.

In Figure 13, we show the $[\text{Fe/H}]$–$[\alpha/\text{Fe}]$ abundance distribution for all individual and coadded abundance measurements of the smooth halo sample. In the top panel, outer ($R_{\text{proj}} > 50$ kpc) halo stars are indicated with dark blue points, and inner halo stars are indicated with cyan points. We find that for the smooth halo, stars in the outer halo are almost exclusively more metal-poor than $[\text{Fe/H}] \sim -1.0$, with a mean metallicity $\langle [\text{Fe/H}] \rangle = -1.94 \pm 0.20$ dex and dispersion $\sigma_{[\text{Fe/H}]} = 0.41$ dex. We measure a mean $[\alpha/\text{Fe}]$ abundance for these stars of $\langle [\alpha/\text{Fe}] \rangle = 0.43 \pm 0.12$ dex, with a dispersion of $\sigma_{[\alpha/\text{Fe}]} = 0.40$ dex. In comparison, the inner ($R_{\text{proj}} < 50$ kpc) halo sample has a significantly higher mean metallicity, with a slightly larger dispersion ($\langle [\text{Fe/H}] \rangle = -1.27 \pm 0.21$ dex, $\sigma_{[\text{Fe/H}]} = 0.61$). We find that the inner halo is less enhanced in $[\alpha/\text{Fe}]$, with a similar dispersion in $[\alpha/\text{Fe}]$ as the outer halo ($\langle [\alpha/\text{Fe}] \rangle = 0.29 \pm 0.08$, $\sigma_{[\alpha/\text{Fe}]} = 0.39$).

6.1.1. Comparison with Other Studies of the M31 Halo

We show the distribution of our outer halo sample compared to other recent, similar samples of the M31 halo in the bottom panel of Figure 13. The outer halo sample presented in Gilbert et al. (2020) is shown in pink, where their sample spans a radial range $46 < R_{\text{proj}} < 110$ kpc. Their sample does not contain any stars likely associated with known substructure, and therefore should represent the smooth outer halo. For comparison, we also show the inner M31 halo ($8 < R_{\text{proj}} < 35$ kpc) sample presented in Escala et al. (2020b), where we have applied the criterion that the probability of a star being associated with substructure is $< 0.5$, to ensure a comparable “smooth halo” sample. The abundance measurements for both the Gilbert et al. (2020) and Escala et al. (2020b) samples were obtained using the same spectral synthesis technique used for this paper, and should therefore be comparable in the sense that the abundance measurements are on the same scale.

Our smooth halo stars closely match the $[\text{Fe/H}]$–$[\alpha/\text{Fe}]$ distribution space spanned by the Escala et al. (2020b) and Gilbert et al. (2020) samples, for the inner and outer halo, respectively. For the inner halo, Escala et al. (2020b) measured a mean metallicity of $\langle [\text{Fe/H}] \rangle = -1.08 \pm 0.04$ dex, and $\langle [\alpha/\text{Fe}] \rangle = 0.40 \pm 0.03$. These measurements are statistically consistent within $1\sigma$ with our inner halo sample ($\langle [\text{Fe/H}] \rangle = -1.27 \pm 0.21$ dex, $\langle [\alpha/\text{Fe}] \rangle = 0.43 \pm 0.12$ dex). For the outer halo, Gilbert et al. (2020) measured a
mean [Fe/H] of $\bar{[\text{Fe/H}]} = -1.92 \pm 0.13$ dex, and a mean $[\alpha/\text{Fe}]$ of $0.30 \pm 0.16$ dex. Again, we find these values to be consistent with what we measure for the smooth outer halo sample ($([\text{Fe/H}]) = -1.94 \pm 0.20, ([\alpha/\text{Fe}]) = 0.43 \pm 0.12$ dex), although we do find a slightly higher $([\alpha/\text{Fe}])$. Between the inner (Escala et al. 2020b) and outer (Gilbert et al. 2020) smooth halo samples, there is evidence for a systematic difference in the mean [Fe/H] between the inner and outer halo. As our sample is consistent with both of these previously published results, we also recover a significant difference in the mean [Fe/H] between the inner and outer smooth halo, with a magnitude of approximately 0.7 dex.

6.1.2. Comparison with M31 dSphs

Gilbert et al. (2020) found that the abundance distribution of their sample of outer halo stars best resembled the abundance distributions of the largest M31 dSphs, And I and And VII. In Figure 14, we show our outer halo sample compared to the individual (filled diamonds) and coadded (open diamonds) abundance measurements for dSphs in three mass ranges from Wojno et al. (2020). The mass range for the dSphs shown is given in the upper right for each panel, respectively, where all mass estimates are sourced from Kirby et al. (2013, 2020; see Table 7 of Wojno et al. 2020 for more details). In the top panel, we show our outer halo abundance distribution compared to two of the most-massive M31 dSphs, And VII (gold, $M_\odot \sim 7.6 \times 10^6$) and And I (red, $M_\odot \sim 1.5 \times 10^7$). In the middle panel, we show the outer halo abundance distribution compared to And III (orange, $M_\odot \sim 6.2 \times 10^5$) and And V (orange, $M_\odot \sim 1.8 \times 10^5$), which represent the middle of the mass range of dSphs presented in Wojno et al. (2020). Finally, in the bottom panel, we show the outer halo abundance distribution compared to And IX (lime, $M_\odot \sim 1.4 \times 10^5$) and And X (cyan, $M_\odot \sim 2.4 \times 10^5$), two of the least-massive dSphs where we have abundance measurements for individual stars.

Compared to inner halo samples from both this work and Escala et al. (2020b; Figure 13), we find that our outer halo sample is more consistent with the abundance distribution of the more-massive dSphs of M31 (top and middle panels of Figure 14). However, the abundance distributions for the more-massive dSphs are slightly more metal-rich and lower in average $[\alpha/\text{Fe}]$, and none of the M31 dSphs with measured
We measure a radial gradient of $-0.0084 \pm 0.0008$ dex kpc$^{-1}$, consistent with results in the literature measured using photometric [Fe/H] estimates. We note there is an offset with respect to the normalization compared to the [Fe/H] gradient measured using photometric [Fe/H] from Gilbert et al. (2014), and we verify that this offset is consistent with the difference between the photometric and spectroscopic [Fe/H] measurements. The persistence of a large-scale metallicity gradient corresponds with a scenario where the bulk of the halo was built up from at least one massive satellite (Cooper et al. 2010), although we acknowledge that there may be significant contributions from less-massive satellites. Additionally, if relatively more-massive satellites with higher metallicities fall into the central regions of the halo, and less-massive satellites interact with the less-dense regions of the halo (Cooper et al. 2010; Tissera et al. 2012), we would expect to see metal-poor, [$\alpha$/Fe]-high stars predominantly in the outer halo.

6.2.2. [$\alpha$/Fe] Gradients

Like [Fe/H], gradients in [$\alpha$/Fe] abundances provide important clues to the star formation history of a galaxy. The ratio of $\alpha$-elements to Fe in a given stellar population is directly linked to the star formation efficiency and supernovae rates (for a through review for this abundance space in the MW, see Matteucci 2021), as $\alpha$-elements are mainly produced in core-collapse SNe by massive, short-lived stars, and low- and intermediate-mass stars explode as Type Ia SNe, producing much higher yields of Fe than core-collapse SNe.

In this work, we find a positive gradient (+0.0030 ± 0.0009) in [$\alpha$/Fe] as a function of projected radius for smooth halo stars when we fit over the full radial range of the sample (see upper-left panel of Figure 5). If we consider only stars possibly associated with known substructures, we do not measure a significant gradient as a function of projected radius (+0.0011 ± 0.0021; $R_{\text{proj}} < 90$ kpc). However, if all M31 stars are included in the fit, the measured [$\alpha$/Fe] gradient remains statistically significant (+0.0027 ± 0.0005, upper-right panel of Figure 5). The strength and significance of the measured gradient in [$\alpha$/Fe] is affected by the stars, and the radial range, included in the fit.

While gradients in [$\alpha$/Fe] as a function of projected radius have been studied primarily in the star-forming disks of galaxies, studies of the MW halo indicate the presence of a negative gradient in [$\alpha$/Fe] (e.g., Fulbright 2002; Nissen & Schuster 2010; Hawkins et al. 2015; Fernández-Alvar et al. 2017). In addition, Conroy et al. (2019) found a flat vertical gradient in [$\alpha$/Fe] for the MW, using a sample of stars spanning a radial range out to 100 kpc, and vertical distance $|z| < 10$ kpc.

However, these studies typically cover a limited range in radius from the center of the MW compared to the range in projected radii for our stars in M31, and therefore we turn to simulations for a more comprehensive comparison. We acknowledge that there are certain limitations when comparing our observational results to simulated galaxies, namely, that the simulations described below do not reach the resolution of individual stars, and therefore these abundance measurements are calculated using "integrated light." Font et al. (2020) noted that there are systematic effects when comparing observational abundance measurements obtained using different methods to
results from simulations. In addition, simulated abundance measurements are subject to systematic effects arising from different methods (e.g., measuring the median or mass-weighted mean for each particle), as well as additional sources of uncertainty in nucleosynthetic yields and supernovae rates. Therefore, we present the comparison here in a qualitative sense to describe general trends.

Using simulations of MW- and M31-mass galaxies, Font et al. (2011) found a slightly positive radial gradient in $[\alpha/Fe]$. An updated version of this analysis using the ARTEMIS simulations (Font et al. 2020) found similar negative [Fe/H] gradients for both the in situ and accreted halo components, with constant $[\alpha/Fe]$ as a function of radius (i.e., no gradient), although there is some indication of a positive trend in the outermost regions of the simulated galaxies. Font et al. (2011) ascribed the presence of a positive gradient in $[\alpha/Fe]$ as a function of $R_{\text{proj}}$ as due to the relative importance of SNe Ia (resulting from intermediate-mass stars) in the inner regions of the galaxy, where SNe II (resulting from massive stars) produce metals at all radii. They found that increasing the rate of SNe Ia in their simulated galaxies increases the steepness of the gradient in $[\alpha/Fe]$ as a function of $R_{\text{proj}}$. The lack of a radial gradient in $[\alpha/Fe]$ can be the result of early accretion across the entire halo, where both the in situ and accreted components have had similar enrichment histories. On the other hand, a negative gradient implies low-$[\alpha/Fe]$ stars in the outer halo compared to the inner halo, which may result from the accretion of satellites with a star formation efficiency such that they have been sufficiently enriched to higher values of [Fe/H] and therefore lower values of $[\alpha/Fe]$.

If we compare the results of these simulations with the most analogous sample in this work (i.e., the gradient fit to all M31 stars, $+0.0027 \pm 0.0005$), we find a positive gradient in $[\alpha/Fe]$ as a function of $R_{\text{proj}}$. However, we note that if we consider only stars at $R_{\text{proj}} < 90$ kpc, we find that the trend in $[\alpha/Fe]$ as a function of $R_{\text{proj}}$ is consistent within $2\sigma$ with being flat ($0.001 \pm 0.0005$ dex kpc$^{-1}$). In our sample, stars at larger projected radii ($R_{\text{proj}} > 100$ kpc) have higher $[\alpha/Fe]$, which increases the measured gradient when the entire radial range is included. The location of these stars in [Fe/H]–$[\alpha/Fe]$ space is most similar to the “in situ” or “canonical halo” population of MW stars (e.g., Hawkins et al. 2015; Hayes et al. 2018); however, at $R_{\text{proj}} > 100$ kpc, these stars would have had to migrate a significant distance outward from the central regions of M31. Therefore, we conclude that these stars are likely to be related to accretion events.

### 6.2.3. Abundance Gradients from Other Tracers

Abundance gradients have also been detected using a variety of tracers, such as HI regions (e.g., Zaritsky et al. 1994), PNe (e.g., Sanders et al. 2012; Bhattacharya et al. 2022), and integrated light spectra of GCs (e.g., Beasley et al. 2005; Colucci et al. 2009, 2014; Sakari et al. 2016; Sakari & Wallerstein 2022). Of these tracers, GCs offer the most appropriate comparison with our outer halo RGB stars, as GCs associated with M31’s halo are found out to distances beyond 50 kpc (Colucci et al. 2014; Sakari et al. 2016; Sakari & Wallerstein 2022).

Sakari & Wallerstein (2022) found that, in general, outer halo GCs ($R_{\text{proj}} > 25$ kpc) are more metal-poor (mean [Fe/H] = $-1.61 \pm 0.40$) than inner halo GCs ($R_{\text{proj}} < 25$ kpc, mean [Fe/H] = $-0.97 \pm 0.60$). In addition, they found that their sample of outer halo GCs are more similar to the smooth halo population, and that the outer halo GCs not associated with any substructure are almost exclusively more metal-poor than [Fe/H] = $-1.5$. This difference between inner and outer halo GCs translates to a metallicity gradient (see their Figure 15), where the value of the gradient is consistent with previous measurements using photometric metallicities (Gilbert et al. 2014), as well as our spectroscopic gradient measurement (Section 6.2).

While this work measures metallicity gradients in the halo of M31, for completeness we also compare our results to the metallicity gradient measured for the M31 stellar disk. Gregersen et al. (2015) used photometric metallicity estimates for old RGB stars in the disk of M31 to measure a radial gradient of $-0.020 \pm 0.004$ dex kpc$^{-1}$. Their sample of RGB stars with photometric metallicity estimates cover a range of 4–20 kpc in projected radius from the center of M31. This disk gradient is $\sim 2.4$ times steeper than the metallicity gradient we measure in M31’s halo.

### 7. Conclusions

In this work, we present newly determined spectroscopic [Fe/H] and $[\alpha/Fe]$ for 160 stars observed in the halo of M31. We classify stars as belonging to either the smooth halo (91 stars), or potentially associated with substructure components, i.e., tidal debris from an accreted population (69 stars). Where we cannot measure abundances for individual stars reliably, we group spectra of different stars together and coadd them. We obtain a total of 118 coadded measurements (62 smooth halo, 56 substructure stars), from a pool of 611 stars without reliable individual abundances. These coadded abundance measurements have been shown to reflect the weighted average of the component stars reliably (Wojno et al. 2020). At large projected radii ($R_{\text{proj}} > 50$ kpc), we obtain measurements for 25 individual stars (as well as 21 coadds from a pool of 111 stars) in the smooth halo, and 20 individual stars (as well as 12 coadds from a pool of 63 stars) possibly associated with substructure components. Prior to this work, only nine stars in the outer halo of M31 ($43 < R_{\text{proj}} < 165$ kpc) had [Fe/H] and $[\alpha/Fe]$ measurements available in the literature (Vargas et al. 2014; Gilbert et al. 2020). We therefore greatly expand on the number of spectroscopic abundance measurements in the M31 halo using this technique, especially at large radii where confirmed M31 halo stars are sparse.

We measure a radial [Fe/H] gradient of $-0.0075 \pm 0.0012$ for the smooth halo. This gradient is consistent with previous results using photometric [Fe/H] (Gilbert et al. 2014), but over a larger radial range. We find a similar gradient for the full M31 halo sample ($-0.0084 \pm 0.0008$), including stars possibly associated with substructure components. Additionally, we find evidence for a significant $[\alpha/Fe]$ gradient in the smooth halo ($+0.0030 \pm 0.0009$) over the entire radial range of our sample ($9 < R_{\text{proj}} < 180$ kpc), using both individual and coadded abundance measurements. We do not find evidence for a gradient when considering only stars possibly associated with substructure. The finding for our smooth halo sample is in contrast to Escala et al. (2020b), where they found no significant $[\alpha/Fe]$ gradient using abundance measurements for individual stars in the radial range $9 < R_{\text{proj}} < 35$ kpc.

Following these gradients, we also find that the distribution of stars in [Fe/H]–$[\alpha/Fe]$ abundance space changes as a function of projected radius from the center of M31. The inner regions of the halo are typically more metal-rich, and less enhanced in $[\alpha/Fe]$.
substructure populations were likely accreted more recently than accreted progenitors.\textsuperscript{2019; Escala et al.2021} The mean distribution of the underlying smooth halo of M31. We possibly associated with tidal debris features with the abundance distribution of the GSS measured in this work, consistent with previous results (e.g., Gilbert et al. 2019; Escala et al. 2021), is indicative of a relatively massive progenitor, adding to the evidence that M31 may have had a major merger much more recently than the MW (e.g., Belokurov et al. 2018; D’Souza & Bell 2018; Hammer et al. 2018; Helmi et al. 2018; Koppelman et al. 2019; Sotillo-Ramos et al. 2022). Stars associated with the GSS substructure, likely caused by a major (4:1 mass ratio) merger a few gigayears ago (D’Souza & Bell 2018; Hammer et al. 2018; Quirk & Patel 2020), are on average more metal-rich, and have a slightly lower mean $\alpha$-Fe compared to the smooth halo at the same $R_{\text{proj}}$ distance. The observed decline in $\alpha$-Fe as a function of [Fe/H] also points to the progenitor of the GSS having an extended star formation history. We see a similar effect in our sample of stars associated with the envelope of the GSS, where the $\alpha$-Fe values of the substructure stars are on average much lower than the smooth halo of M31.

When we consider only stars at large projected radii (“outer halo” stars, Section 6), we find they are almost exclusively more metal-poor than [Fe/H] $\leq -1.0$, and are enhanced with respect to $\alpha$-Fe. We find that our sample of inner halo stars is on average more metal-rich, with a slightly broader distribution in [Fe/H] compared to the outer halo stars. If we compare our sample of stars in the outer halo, we find, as in Gilbert et al. (2020), that the abundance distribution of smooth outer halo stars is consistent with the abundance distributions of the more-massive dSphs of M31 (e.g., And I, III, V, VII). However, we find that the abundance distribution of the smooth outer halo stars is not fully represented by any one of the surviving dSphs, implying that the stars in the metal-poor, [α/Fe]-enhanced region of the parameter space may have been accreted through multiple separate merger events.

While it is still difficult to accurately reconstruct the chemical evolution pathways within the progenitors of current-day substructure, this work shows that the halo of M31 is incredibly complex not only kinematically, but also chemically. Obtaining additional spectroscopic abundance measurements covering the entirety of the M31 halo is outside of the reach of the current generation of multiobject spectroscopic instruments (although see Dey et al. (2023) for a recent spectroscopic study of M31 halo stars with $R \sim 2000–5000$), but may be achievable in the next generation of large-scale spectroscopic surveys, such as the Subaru Prime Focus Spectrograph (PFS).

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This research made use of Astropy, a community-developed core Python package for Astronomy (Astropy Collaboration et al. 2013, 2018).\textsuperscript{17}

\textit{Facility:} Keck:II (DEIMOS).

\textit{Software:} Astropy (Astropy Collaboration et al. 2013), Matplotlib (Hunter 2007), numpy (van der Walt et al. 2011), scipy (Virtanen et al. 2020), emcee (Foreman-Mackey et al. 2013).

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