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Physical controls on orographic cirrus inhomogeneity

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Abstract

Optical depth distributions ($P(\sigma)$) are a useful measure of radiatively important cirrus (Ci) inhomogeneity. Using a parcel model with binned ice microphysics and kinematic trajectories from a mesoscale weather model (MM5), we assess physical controls on Ci $P(\sigma)$ during an orographic Ci case study. On 19 April 2001, satellite imagery revealed Ci formation in the lee of the Southern Rocky Mountains and Ci advection along a broad upper level ridge. Above Lamont, Oklahoma (USA), lidar observations indicated a broad Ci $P(\sigma)$. Along MM5 trajectories associated with the observed Ci, homogeneous freezing and mesoscale variability in vertical velocities led to broad modeled $P(\sigma)$ and variability in modeled Ci cloud lifetimes. The addition of background ice nuclei concentrations ($N_{IN} = 0.03 \, \text{cm}^{-3}$) to air parcels had little impact on modeled Ci $\sigma$ variability. The presence of background $N_{IN}$ did increase cloud cover by increasing the frequency of small $\sigma$ Ci. These results highlight the importance of homogeneous freezing and mesoscale vertical velocity variability in controlling Ci $P(\sigma)$ shapes along realistic upper tropospheric trajectories.

1 Introduction

1.1 Background

Cirrus clouds (Ci), layer clouds that are entirely glaciated, are often optically inhomogeneous. Neglecting Ci optical depth ($\sigma$) inhomogeneity can lead to large biases in computed radiative fluxes (Fu et al., 2000; Carlin et al., 2002). One useful measure of Ci inhomogeneity is an optical depth distribution $P(\sigma)$, i.e., the fraction of $\sigma$ occurring at a given $\sigma$. Understanding physical controls on Ci $P(\sigma)$ should improve representation of radiative fluxes in weather and climate models.

In general, Ci $\sigma$ can be approximated as:

$$\sigma = 2\pi R_{eff}^2 N_{ice} \Delta Z \quad (1)$$
where $R_{\text{eff}}$ is the ice crystal effective radius [m], $N_{\text{ice}}$ is number concentration of ice crystals [$m^{-3}$], and $\Delta Z$ is the Ci cloud layer thickness [m].

From Eq. (1), we find that for a fixed ice $R_{\text{eff}}$ and $\Delta Z$, Ci $\sigma$ are determined primarily by $N_{\text{ice}}$. Therefore, understanding physical controls on Ci $N_{\text{ice}}$ is a first-step towards understanding physical controls on Ci $P(\sigma)$.

Kärcher and Ström (2003) and Hoyle et al. (2005) concluded that homogeneous freezing and small scale variability (frequencies ($\nu$ [hr.$^{-1}$]) up to 10 h$^{-1}$ or spatial scales <11 km) in vertical velocity ($w$ [m s$^{-1}$]) controlled $N_{\text{ice}}$ distributions measured during the INCA and SUCCESS field campaigns. Haag and Kärcher (2004) found that background number concentrations of ice nuclei ($N_{IN}$) reduced modeled $N_{\text{ice}}$, but that IN presence did not significantly alter overall Ci properties and formation locations. Kay (2006) noted that observed $N_{IN}$ ($N_{IN} <0.1 \text{ cm}^{-3}$ (DeMott et al., 2003; Rogers et al., 1998)) and homogeneous freezing at weak synoptic-scale $w$ ($w<<5 \text{ cm s}^{-1}$ (Mace et al., 2001)) could not explain the mean observed $N_{\text{ice}}$ at Lamont, Oklahoma (USA) ($\bar{N}_{\text{ice}}=0.1 \text{ cm}^{-3}$, Mace et al., 2001). Taken together, these studies suggest that observed Ci $N_{\text{ice}}$ can be largely explained by homogeneous freezing occurring at a range of $w$. These studies also imply that heterogeneous freezing alone cannot explain observed Ci $N_{\text{ice}}$.

Kay et al. (2006) (hereafter K06) assessed physical controls on Lagrangian $P(\sigma)$ along constant lifting trajectories. For a typical range of $w$, temperatures ($T$ [K]), and $N_{IN}$, $\bar{\sigma}$ and $P(\sigma)$ shape depended primarily on $w$. The sensitivity of $\bar{\sigma}$ to $w$ resulted for two reasons: 1) As $w$ increased, Ci $N_{\text{ice}}$ increased, $R_{\text{eff}}$ decreased, and the initial $\sigma$ increased (see Eq. 1). 2) As $R_{\text{eff}}$ decreased, fallout timescales ($\tau_{\text{fallout}}$ [s]) and cloud lifetimes increased. In other words, the $w$ during freezing controlled both the initial $\sigma$ and the $\sigma$ evolution. In contrast, the addition of IN to lifting parcels had a limited influence on modeled $\sigma$. The addition of observed $N_{IN}$ only reduced $\bar{\sigma}$ and modified $P(\sigma)$ with large $w$. With small $w$, IN had little influence on the calculated $\bar{\sigma}$ and $P(\sigma)$ because IN quickly fell out of the parcel, and because the $N_{\text{ice}}$ generated by homogeneous freezing at low $w$ were comparable to observed $N_{IN}$. 

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Given the importance of $w$ to Ci $N_{\text{ice}}$ and $P(\sigma)$, the influence of realistic $w$ sequences on Ci formation and evolution should be evaluated. Unfortunately, it is difficult to predict air flow and measure $w$ along Ci evolution pathways. With the exception of wave cloud studies (e.g., INTACC (Field et al., 2001), FIRE II (Heymsfield and Miloshevich, 1995)), there is a dearth of Lagrangian $w$ observations. As a substitute for measuring Lagrangian $w$ in the atmosphere, previous studies (e.g., Hoyle et al., 2005; Haag and Kärcher, 2004) have statistically constructed Lagrangian $w$ trajectories. In these studies, observed distributions of small-scale $w$ were superimposed on Lagrangian displacement trajectories derived from large-scale atmospheric models (horizontal resolution >40 km). Because Lagrangian $w$ measurements are difficult to obtain, and because statistically constructed $w$ trajectories are not necessarily realistic, kinematic trajectories extracted from mesoscale weather models (4 km < horizontal resolution <40 km) could serve as a useful proxy for Lagrangian $w$ observations. Mesoscale weather model trajectories capture mesoscale $w$ variability ($2 \text{ h}^{-1} < \nu < 10 \text{ h}^{-1}$) and provide a realistic and self-consistent measure of Lagrangian $w$ evolution.

1.2 Study goals and organization

In this study, we investigate physical controls on orographic Ci $P(\sigma)$ using the K06 parcel model and $w$ trajectories derived from the PSU/NCAR mesoscale model (MM5) (Grell et al., 1994). We selected an orographic Ci case study because mountainous terrain provides a natural laboratory for investigating the influence of mesoscale ($2 \text{ h}^{-1} < \nu < 10 \text{ h}^{-1}$) $w$ variability ($w = 1–300 \text{ cm s}^{-1}$, cooling rates $= 1–100 \text{ K h}^{-1}$) on Ci $P(\sigma)$, and because orographic Ci are often missed by climate models (Dean et al., 2005).

In Sect. 2, we introduce the orographic Ci case study using observations. In Sect. 3, we present and evaluate the meteorology and $w$ forecasted by MM5. In Sect. 4, we describe both our methods for estimating $\sigma$ evolution with the K06 parcel model and our trajectory parcel model experiments. Section 5 contains our results: We evaluate the influence of $w$ and IN on Ci $P(\sigma)$ calculated along realistic upper tropospheric
trajectories. We compare parcel model Ci to the Ci generated by a standard MM5 bulk microphysics scheme, the Reisner II scheme (Reisner et al., 1998). Their inter-comparison is interesting because the Reisner II scheme neglects the influence of $w$ on Ci $N_{\text{ice}}$. Finally, we assess which physical factors could explain the observed Ci formation and broad $P(\sigma)$. Section 6 contains a summary and discussion of our results.

2 19 April 2001 Ci observations

On 19 April 2001, orographic Ci formation and evolution was observed by the GOES infrared satellite and a vertically pointing Raman lidar located at Lamont, Oklahoma (OK), hereafter Lamont (Fig. 1). From 06:00 to 16:00 UTC, orographic Ci formed in the lee of the Southern Rocky Mountains. The Ci were then advected East with the upper level winds. Approximately 5 to 6 h after formation, the Ci were observed by the lidar above Lamont.

The lidar-observed Ci had a constant cloud top height of approximately 12 km, but a cloud base that varied from 6.5 to 11 km (Fig. 1). Two independent $\sigma$ retrievals, one based on emissivity shape in the atmospheric window retrieved from Atmospheric Emitted Radiance Interferometer (AERI) observations (Turner, 2005), and the other based on Beers law and the lidar backscatter below and above cloud, were generally consistent when $\sigma<3$. Retrieved Ci $\sigma$ increased monotonically from 06:00 to 12:00 UTC and then varied from $\sigma<0.1$ to $\sigma\sim3$ (Fig. 2). From 12:00 to 24:00 UTC, $\sigma$ variability resulted in a broad $P(\sigma)$ (Fig. 2). Although the lidar observations do not reveal the influence of $N_{\text{ice}}$ and $R_{\text{eff}}$ on the observed $\sigma$, they do suggest that variable $\Delta Z$ contributed to the observed broad $P(\sigma)$ (see Eq. 1).
3 19 April 2001 MM5 forecast

3.1 MM5 Methods

We ran the MM5 with three nested domains for the 19 April 2001 orographic Ci event both to forecast the meteorology, and to enable calculation of Lagrangian $w$ trajectories (Fig. 3, Table 1). All MM5 domains included the Front Range of the Rocky Mountains, where the Ci formed, and Lamont, where the Ci passed overhead (Fig. 1).

3.2 MM5 meteorology

At 12:00 UTC on 19 April 2001, the MM5 forecasted a broad upper-level ridge over the central United States, a low pressure system developing in Montana, and a trough in the lee of the Rocky Mountains (Fig. 4). Both the developing Montana low and the lee trough contributed to a weak North-South trending warm front. A cross section of equivalent potential temperatures shows the lee trough, a cold front aloft above the Rockies, and a warm front approaching Northern OK (Fig. 4). Circulation vectors with the mean motion of the cold front removed demonstrate that air above 8 km had net westerly air flow.

Although the MM5 forecast (Fig. 4) was broadly consistent with the National Weather Service (NWS) reanalysis at 850 mb and 500 mb, the MM5 had a stronger and tighter Montana low, and a reduced gradient in, and lower overall, 500 mb geopotential heights over the Rockies. In the South Central USA, these model geopotential height biases indicate that the MM5 forecast had lower wind speeds over the Rockies, and weaker frontal lifting than what was observed.

3.3 MM5 vertical velocities

Above the Southern Rockies in central New Mexico and Colorado, MM5 forecasted vertically propagating orographic gravity waves with large ($w>100$ cm s$^{-1}$) and variable $w$ (Fig. 5). The strongest vertical motions resulted from 12:00 to 15:00 UTC when the
upper level winds were perpendicular to the Rockies and the cold front aloft approached the Western edge of the lee trough. Downwind of the Rockies, \( w \) were generally small (\( w < 30 \text{ cm s}^{-1} \)).

Using the MM5 wind fields, we calculated Lagrangian \( w \) trajectories associated with the observed Ci formation and evolution (Table 2). Our calculations indicate that air from Eastern New Mexico and Colorado traveled over the Southern Rockies, and arrived above Lamont in approximately 8 h.

The MM5 domain resolution influenced the amplitude and spatial scale of \( w \) variability along the trajectories (Fig. 6). Trajectories derived from the MM5 domain with 4-km spatial resolution (D4km) had a larger range of \( w \) than trajectories derived from the MM5 domain with 36-km spatial resolution (D36km). The D4km trajectories also had greater spectral power at mesoscale frequencies (spatial equivalent 20–60 km) than the D36km trajectories. Neither set of trajectories had small-scale variability in \( w \) because neither domain resolved dynamics occurring at small scales (\( \nu > 6 \text{ h}^{-1} \), spatial equivalent <18 km).

The sensitivity of the modeled \( w \) to MM5 domain resolution and the lack of \( w \) observations made it difficult to quantitatively validate the MM5-forecasted \( w \). As a result, we qualitatively assessed the MM5 \( w \) forecasts within the context of the two main drivers of orographic wave development: the mountain range topography and the upwind atmospheric stability and wind profile (Durran, 2003).

Mountain wave theory suggests that given the large width of the Front Range, vertically propagating hydrostatic waves should result for most atmospheric stability and wind profiles (Durran, 2003). The D4km \( w \) are consistent with this theory (Fig. 5). With the relatively steep leeward slope of the Front Range, idealized calculations suggest hydrostatic gravity waves could generate positive displacement at Ci heights (see Figure 20.11 in Durran (2003)). At upper levels, MM5 forecasted persistent positive \( w \) at heights of 6–12 km in the lee of the Rockies (Fig. 5).

To evaluate the representation of the upstream wind and stability profiles, we compared the modeled and observed soundings at Albuquerque, New Mexico (ABQ)
(Fig. 7, Fig. 3). The MM5 ABQ sounding was qualitatively similar to the observed ABQ sounding. Both soundings had a stable atmospheric potential temperature profile and increasing wind speed with height. Differences between the MM5 and the observed ABQ sounding included: 1) the MM5 sounding was more stable and 2) the MM5 ABQ sounding had less vertical wind speed shear above 8 km. Despite these differences, the MM5 representation of wind and stability profiles provided confidence in the forecasted gravity wave development.

4 Parcel model methods

4.1 Conceptual framework

In this study, we evaluate Ci processes occurring along Lagrangian w trajectories using the K06 parcel model and a simple conceptual framework (Fig. 8).

The key assumption in our conceptual framework is that processes occurring in an ice formation region near cloud top control P(σ) shape. We model freezing, vapor diffusion, and fallout occurring in this ice formation region with the K06 parcel model. We then calculate Ci σ evolution using Eq. (1) by linearly scaling the ice formation region $R_{\text{eff}}$ and $N_{\text{ice}}$ over the entire cloud depth and by assuming $\Delta z = 1000 \text{ m}$. Finally, we calculate Ci P(σ) and other distributions such as P($N_{\text{ice}}$) over the duration of the modeled Lagrangian evolution.

Within our conceptual framework, it is easy to understand and to quantify interactions between complex dynamics and Ci microphysical processes. In an adiabatic parcel model following a Lagrangian displacement trajectory, the time and location of a new freezing event (i.e., when $\frac{dN_{\text{ice}}}{dt}$ increases above a specified threshold) is controlled both by the initial conditions, which set the total displacement required to start freezing, and by the displacement trajectory. If homogeneous freezing begins, $w$ and $T$ control the maximum homogeneous nucleation rate ($J_{\text{hom-max}} [m^{-3} s^{-1}]$) and the resulting $N_{\text{ice}}$. If heterogeneous freezing begins, $N_{IN}$ and the IN freezing threshold deter-
mine the resulting $N_{\text{ice}}$. Once Ci form, their $\sigma$ evolution and $P(\sigma)$ shape are determined by the shortest microphysical and dynamical timescales (see K06). Because the parcel model is a zero-dimensional model, the computational requirements for estimating interactions between realistic dynamics derived from a three-dimensional numerical weather model and binned microphysics are minimal.

Despite the described advantages, there are limitations associated with our methodology for estimating Ci $\sigma$ evolution (see also K06 and Kay, 2006). For simplicity, we use a constant depth of the ice formation region ($H$ [m]) and a constant $\Delta z$. Neither of these assumptions is completely realistic. First, 100 m is a reasonable, but ad hoc, estimate for $H$. Cloud evolution is sensitive to $H$ and vertically resolved cloud processes would be more realistic. Fortunately, $\sigma$ trends and $P(\sigma)$ shapes are largely independent of $H$. Second, using a constant scaling of the formation region properties to obtain an integrated Ci $\sigma$ cannot always be justified. For example, $\Delta z$ variability often contributes to $\sigma$ variability. Because we assume a constant $\Delta z$, we can only incorporate $\sigma$ variability associated with variability in $w$ and initial conditions such as $N_{IN}$. A more complicated model could incorporate the influence of $\Delta z$ variability on $\sigma$ variability.

4.2 Parcel model runs

Guided by the observed Ci cloud top and timing (Fig. 1), we focused our Ci modeling efforts on trajectories ending 12 km above Lamont (Table 2). We calculated Ci evolution with variable initial conditions and $w$ trajectories (Table 3). By comparing $P(\sigma)$ calculated along $w$ trajectories derived from the D36km and D4km MM5 domains, we evaluated the influence of mesoscale $w$ variability and $w$ amplitude on Ci formation and evolution. We also evaluated the effect of IN on Ci $P(\sigma)$ by initializing parcels with either a fixed background concentration based on observations ($N_{IN} = 0.03$ cm$^{-3}$) or the $N_{IN}$ predicted by Meyers et al. (1992), a commonly-used model IN parameterization in which the $N_{IN}$ increases exponentially with the vapor supersaturation with respect to ice.
5 Results

5.1 Overview of results

The Lagrangian dynamical forcing along the MM5 $w$ trajectories revealed large-scale cooling and mesoscale variability in $w$ in the lee of the Rockies. Both the kinematic forcing and the initial conditions affected Ci processes modeled along the Lagrangian trajectories. Our parcel model results demonstrate that mesoscale $w$ variability associated with orographic gravity waves broadened Ci $P(\sigma)$ shape. In contrast, the addition of typical $N/N_i$ to parcels had a limited influence on modeled Ci $\sigma$ variability, but did increase overall modeled Ci cloud cover. Finally, the inhomogeneity, but not the timing, of the observed Ci was reproduced by our Ci parcel modeling along MM5 trajectories.

5.2 Lagrangian forcing

Lagrangian $T$ and $w$ time-time plots from the D4km MM5 domain show the forcing important for Ci formation and evolution on 19 April 2001 (Fig. 9). All air parcels traveled over the high topography of the Southern Rocky Mountains between evolution times $-7$ and $-5$ h, i.e., 5 to 7 h before arrival at Lamont. In the lee of the Rocky Mountains, air parcels experienced cooling, and variable $w$ associated with the vertically propagating orographic gravity waves (Fig. 5). For the last 4 h prior to arrival at Lamont, air parcels had small vertical motions ($w<30\text{ cm s}^{-1}$). Widespread cooling occurred between evolution times $-3$ and $-2$ h, while warming occurred along trajectories in the two hours prior to arrival above Lamont.

5.3 Parcel model Ci

Consistent with observations (Fig. 1), cooling in the lee of the Rockies resulted in parcel model Ci formation from 06:00 to 16:00 UTC, i.e., between evolution times $-6$ and $-4$ h for trajectories arriving above Lamont from 12:00 to 20:00 UTC (Fig. 10). Variability in the large-scale cooling, the mesoscale $w$ amplitude and timing, and the
initial conditions resulted in a range of parcel modeled Ci formation times, \( N_{\text{ice}} \), \( \sigma \), and cloud lifetimes along the Lagrangian trajectories. From the parcel model Ci results, three general Ci formation and evolution sequences could be categorized by arrival time at Lamont:

1. Along trajectories arriving from 12:00 to 14:00 UTC, Ci formed by homogeneous freezing at evolution time –5 h, but Ci then sublimated in descending motions. After a cloud-free period, a second homogeneous freezing event occurred at evolution time –3 h and these Ci persisted to Lamont.

2. Along trajectories arriving from 15:00 to 20:00 UTC, Ci formed from evolution time –5 to –3 h. Variability in \( w \) led to a range of \( N_{\text{ice}} \) and cloud lifetimes. Only the trajectories with large \( N_{\text{ice}} \) and limited descending motion persisted over many hours and arrived at Lamont.

3. Along trajectories arriving from 21:00 to 24:00 UTC, Ci formed from evolution time –8 to –7 h, but few Ci formed in the lee of the Rockies, and no Ci arrived at Lamont.

The addition of background IN to air parcels resulted in changes to the timing and magnitude of homogeneous freezing along individual trajectories; however, the overall location of cloud formation in the lee of the Rockies, the variability in \( N_{\text{ice}} \) and cloud lifetimes, and the quantity of Ci arriving at Lamont were not altered by the addition of background IN (Fig. 10).

Both \( N_{\text{ice}} \) variability and cloud lifetime variability were robust features of the parcel model Ci. In contrast, the Reisner II Ci had limited variability in \( N_{\text{ice}} \) and Ci cloud evolution (Fig. 11). These differences suggest that while the large-scale forcing controlled the location of Ci formation, homogeneous freezing at locally variable \( w \) produced the modeled \( N_{\text{ice}} \) and Ci evolution variability.

Because changes along individual or even hourly trajectories are not necessarily representative of overall changes, we statistically assessed the influence of mesoscale \( w \) variability and \( N_{IN} \) specification on parcel model Ci by comparing \( P(\sigma) \) and \( P(N_{\text{ice}}) \) calculated along all 266 Lagrangian trajectories.
Comparison between $P(\sigma)$ and $P(N_{\text{ice}})$ derived along all of the D36km and D4km trajectories illustrates the influence of mesoscale $w$ variability and $w$ amplitude on Ci properties (Fig. 12). Along D4km trajectories, large $w$ associated with mesoscale $w$ variability broadened $P(\sigma)$ and shifted $P(N_{\text{ice}})$ towards large values. Given that large $N_{\text{ice}}$ lead to long $\tau_{\text{fallout}}$ and long cloud lifetimes, we expected more cloud cover along the D4km trajectories than along the D36km trajectories. We found the opposite: D4km trajectories had 3% less cloud cover than D36km trajectories. Owing to their differing spatial resolutions, the D36km and D4km domains had different representations of the large-scale cooling and gravity wave evolution in the lee of the Rockies. Indeed, both the amplitude and the frequency structure of Lagrangian $w$ varied with the spatial resolution of the MM5 domain (Fig. 6). In the end, our analysis could not isolate the influence of mesoscale $w$ variability on cloud lifetimes and cloud cover from these systematic differences related to the spatial resolution of the resolved dynamics.

Adding $N_{\text{IN}}$ to parcels increased Ci cloud cover along the Lagrangian trajectories from 25% ($N_{\text{IN}} = 0$) to 30% for background $N_{\text{IN}}$ and to 32% for (Meyers et al., 1992) $N_{\text{IN}}$ (Fig. 12). This cloud cover increase occurred only for optically thin Ci and resulted because heterogeneous freezing occurred at a lower $RH_{\text{ice}}$ than homogeneous freezing (see Table 3).

The impact of IN on optically thick Ci depended on $N_{\text{IN}}$. Due to scavenging and their relatively low concentrations, background IN had little impact on the large $\sigma$ and large $N_{\text{ice}}$ Ci that formed by homogeneous freezing. In contrast, the use of the Meyers et al. (1992) parameterization resulted in a large addition of $N_{\text{IN}}$ to parcels and a decrease in the occurrence of large $N_{\text{ice}}$ and large $\sigma$ Ci. The Meyers et al. (1992) parameterization produced more IN than are typically observed in the atmosphere (Meyers $N_{\text{IN}} > 0.3 \text{ cm}^{-3}$). Therefore, we suggest that our background $N_{\text{IN}}$ modeling results are more likely to represent the typical influence of IN on Ci.
5.4 Comparison of modeled and observed Ci

Both the parcel model and Reisner II scheme reproduced the observed orographic Ci formation in the lee of the Rockies; however, both models failed to reproduce the observed Ci presence above Lamont. The lidar depolarization showed Ci occurring continuously from 08:00 to 24:00 UTC (Fig. 1), yet both the parcel model (Fig. 10) and Reisner II (Fig. 11) produced no Ci above Lamont after 16:00 UTC.

Differences between modeled and observed horizontal advection may have contributed to a lack of modeled Ci presence above Lamont. At a height of 12 km, the MM5 horizontal wind speeds were up to 10 m s$^{-1}$ smaller than observed horizontal wind speeds (Fig. 7). For a fixed Ci cloud lifetime, increasing the horizontal wind speed could alter orographic Ci presence above Lamont. For example, an increase in model advection speeds may have allowed parcel model Ci to persist farther from the Rockies and to arrive above Lamont from 16:00 to 20:00 UTC (Fig. 10). Yet, horizontal advection speed cannot entirely explain differences between observed and modeled Ci presence. The GOES observations indicate that Ci persisted after passing above Lamont (Fig. 1).

A moisture deficit could explain the differences between the modeled and observed Ci presence. Modeled $RH_{\text{ice}}$ above Lamont were <100% after 15 UTC, which promoted sublimation of the orographic Ci and inhibited new freezing events (Fig. 13). Low $RH_{\text{ice}}$ resulted from net subsidence (warming) in the two hours before trajectories arrived at Lamont (Fig. 9). The model moisture deficit could have resulted because the MM5 forecast did not adequately capture warm frontal lifting throughout the South Central USA. The reduced southern extent of Montana low in the MM5 forecast as compared to the NWS reanalysis supports this hypothesis.

Given modeled $RH_{\text{ice}}$<100%, it is not surprising that few model Ci arrived at Lamont. With modeled $RH_{\text{ice}}>100\%$, more orographic Ci may have survived and arrived at Lamont. In addition, only modest lifting is required for parcels near ice saturation to reach a homogeneous freezing threshold. If model parcels were lifted an additional 300 to
400 m, new homogeneous freezing events could have occurred and $w$ variability could have resulted in variable $N_{\text{ice}}$.

Despite obvious differences between the observed and modeled Ci presence, model Ci did form in the lee of the Rockies and were advected to Lamont (Fig. 10, Fig. 11). By comparing the observed and modeled Ci properties (Table 4), we found that the parcel model helped explain the Ci observations in the following ways:

1. Observed $\Delta Z$ variability clearly contributed to the observed broad $P(\sigma)$ (Fig. 2); however, the observed broad $P(\sigma)$ at Lamont (Fig. 2) could also be partially explained by variable $N_{\text{ice}}$ resulting from homogeneous freezing at variable $w$. Although the modeled $P(\sigma)$ (Fig. 12) are not coincident in time and space with the $P(\sigma)$ observations at Lamont, broad modeled $P(\sigma)$ along trajectories resulted from homogeneous freezing occurring at variable $w$.

2. Large $N_{\text{ice}}$ resulted in long parcel modeled Ci lifetimes. Thus, the parcel model could help explain the observed persistence of Ci over many hours in the GOES imagery.

### 6 Conclusions

Using self-consistent Lagrangian trajectories derived from a mesoscale weather model and a parcel model with binned ice microphysics, this study evaluated the influence of mesoscale $w$ and IN presence on Ci $N_{\text{ice}}$, and inhomogeneity during an orographic Ci case study. The primary findings were:

- When mesoscale variability (along-path fluctuations with timescales of $2 \text{ h}^{-1} < \nu < 10 \text{ h}^{-1}$) in $w$ affected homogeneous freezing, $P(\sigma)$ derived along Lagrangian trajectories were broad. Broad $P(\sigma)$ resulted because homogeneous freezing driven by variable $w$ led to variable $N_{\text{ice}}$, variable $\sigma$, and variable Ci lifetimes.
The addition of IN to air parcels increased cloud cover along Lagrangian trajectories by 5 to 7%, depending on the $N_{IN}$ and IN freezing threshold. Whereas background $N_{IN}$ ($N_{IN}=0.03 \text{ cm}^{-3}$) presence had little influence on the occurrence of large $\sigma$, the presence of large $N_{IN}$ ($N_{IN}>0.3 \text{ cm}^{-3}$), resulting from use of Meyers et al. (1992) parameterization, decreased the occurrence of large $\sigma$ by suppressing homogeneous freezing. Because the Meyers et al. (1992) parameterization produced more IN than are typically observed ($N_{IN}<0.1 \text{ cm}^{-3}$ (DeMott et al., 2003; Rogers et al., 1998)), the background $N_{IN}$ modeling results are representative of what occurs in the atmosphere.

All models predicted fewer Ci than were observed. Low humidities along modeled trajectories, which were attributed to a lack of MM5 frontal lifting, could explain differences in modeled and observed Ci. Nevertheless, the parcel model Ci helped explain observed Ci inhomogeneity in the following sense: 1) Broad observed $P(\sigma)$ could be partially explained by variable $N_{ice}$ arriving along parcel model Ci trajectories, 2) Large $N_{ice}$ predicted by the parcel model resulted in long Ci lifetimes and could explain the persistence of Ci over many hours.

Although there are limitations associated with using an adiabatic parcel model and trajectories to represent Ci processes and properties, the results from this study demonstrate clear connections between mesoscale $w$, Ci $N_{ice}$, and Ci $P(\sigma)$. Our results support and extend the results of Kärcher and Ström (2003); Hoyle et al. (2005); Haag and Kärcher (2004), who suggested that $w$ variability and homogeneous freezing generate $N_{ice}$ variability in the atmosphere.

The primary goal of this study was to illustrate the influence of mesoscale $w$ and $N_{IN}$ variability on Ci $P(\sigma)$ along numerous realistic Lagrangian trajectories. Therefore, we were not alarmed to find deviations between modeled and observed Ci presence. A mesoscale model forecast is an initial value problem with a single realization. We could have generated MM5 forecasts until we reproduced the observed Ci presence, but a detailed reproduction of the observations was not our goal. The observations...
were invaluable because they helped us identify 19 April 2001 as a good case study, not because they provided a benchmark for evaluating the ability of models to exactly reproduce observations.

Given the limitations of this study, and that this is only a single case study, the influence of \( w \) and IN on Ci cloud properties should be explored further. In particular, modeling Ci evolution along trajectories derived from models that resolve \( w \) variability at small spatial scales (\( \nu > 6 \text{ h}^{-1} \)) would be useful. In addition, including the effects of variable \( \Delta z \) on \( P(\sigma) \) and comparing the influence of \( \Delta z \) with the influence of \( w \) highlighted by this study would be interesting. Finally, we recommend investigation of the parallels between the \( w \)-\( N_{\text{ice}} \)-cloud lifetime-cloud cover connections described in this study and the indirect effects of aerosols on stratus albedos, lifetimes, and cloud cover (e.g. Twomey, 1974; Albrecht, 1989).

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### Table 1. MM5 V3.7.3 configuration.

| MM5 model specification          | Value                                      |
|----------------------------------|--------------------------------------------|
| Forecast duration                | 36 h.                                      |
| Forecast start                   | 12:00 UTC 18 April 2001                    |
| Domain spatial resolution        | 36 km, 12 km, 4 km                         |
| Domain temporal resolution       | 240 s, 80 s, 27 s                          |
| Vertical extent                  | 50 levels, 0 to 100 km                     |
| Vertical resolution              | 500 m from 6 to 13 km                      |
| Initialization                   | NCEP/NCAR Reanalysis                      |
| Microphysics parameterization    | Reisner II                                 |
| Cumulus parameterization         | Kain Fritsch                              |
| Shallow convection option        | None                                       |
| Radiation parameterization       | CCM2                                       |
| Nudging                          | None                                       |
Table 2. Lagrangian MM5 trajectories.

| Trajectory parameter                      | Value                                      |
|-------------------------------------------|--------------------------------------------|
| MM5 domain                                | D36km, D4km                                |
| Duration                                  | 8 h.                                       |
| Temporal resolution                       | 3.6 min.                                   |
| End time above Lamont                     | 08:00 to 24:00 UTC                         |
| End height above Lamont                   | 12 km                                      |
| Total number                              | 266                                        |
Table 3. Description of parcel model (PM) experiments: All PM experiments are named as follows: PM_MMM5Domain_INparameterization(if applicable). All parcels were initialized with sulfuric acid aerosols (dry mass = 10^{-16} \text{ kg}, N_{aer} = 100 \text{ cm}^{-3}). Parcel initial conditions (T, RH_{\text{ice}}, P) and w trajectories were derived from the indicated MM5 domain. All background IN froze at a shifted water activity equivalent to freezing at RH_{\text{ice}}=130\% (see Kärcher and Lohmann, 2003).

| Experiment name | MM5 domain | IN            |
|-----------------|------------|---------------|
| PM_D4km         | D4km       | none          |
| PM_D4km_IN      | D4km       | Background IN |
| PM_D4km_Meyers  | D4km       | Meyers et al. (1992) |
| PM_D36km        | D36km      | none          |
Table 4. Model vs. observed variability in Ci properties above Lamont from 08:00 to 24:00 UTC on 19 April 2001. Model values are only included for model IWC >0.01 m m$^{-3}$.

| Source           | $N_{\text{ice}}$ cm$^{-3}$ | $P_{\text{eff}}$ µm | $\sigma$ dimensionless |
|------------------|-----------------------------|---------------------|------------------------|
| PM_D4km          | 0.01–3.05                   | 1–25                | 0.01–0.7               |
| PM_D4km_IN       | 0.01–2.71                   | 6–30                | 0.03–0.7               |
| PM_D4km_Meyers   | 0.001–1.04                  | 5–25                | 0.01–0.3               |
| ReisnerII_D4km   | 0.02–0.08                   | 25–36               | NA                     |
| Observed         | NA                          | NA                  | 0–3                    |
Fig. 1. Infrared satellite and lidar depolarization observations on 19 April 2001: (A) GOES infrared satellite image time series. Low brightness temperatures indicate high cloud tops. (B) Vertically pointing lidar depolarization ratio observations from Lamont. High depolarization ratios (>10%) indicate ice.
Fig. 2. 19 April 2001 $\sigma$ observations: (A) $\sigma$ time series. Time series of Ci $\sigma$ based on two independent retrieval methods (AERI, lidar). (B) 12-h lidar-derived $P(\sigma)$. 
Fig. 3. MM5 domain configuration used for the 19 April 2001 forecast.
Fig. 4. MM5 meteorology at 12:00 UTC on 19 April 2001 (A) 500 mb temperatures and geopotential heights (B) 850 mb temperatures and geopotential heights. (C) Cross section through AA-AA. Circulation vectors have the mean speed of the cold front removed (12.7 m s⁻¹).
Fig. 5. MM5 vertical velocities at 12:00 UTC on 19 April 2001. (A). D4km 300 mb w (B) D4km w cross section. Location of cross section BB-BB is indicated on (A).
Fig. 6. The effect of MM5 domain resolution on vertical velocity amplitude and frequency structure along Cj Lagrangian evolution pathways. A horizontal wind speed of 30 m s$^{-1}$ was assumed in all spatial equivalence calculations.
Fig. 7. ABQ 04/19/2001 12 UTC sounding comparison: (A). MM5 D4km vs. observed stability profile (B). MM5 D4km vs. observed wind speed profile.
**Fig. 8.** Ci conceptual framework.
Fig. 9. Temperature and vertical velocity along Lagrangian trajectories derived from the D4km MM5 domain: These time-time plots show the Lagrangian evolution of the MM5 kinematic forcing on air parcels arriving 12 km above Lamont. The y-axis indicates the parcel arrival time at Lamont. The x-axis indicates the evolution time, i.e., the time before parcel arrival at Lamont.
Fig. 10. Parcel model Ci along hourly trajectories: \( N_{\text{ice}} \) and \( \sigma \) from the parcel model are plotted along Lagrangian trajectories ending every hour 12 km above Lamont. White indicates no cloud was present (IWC < 0.01 mg m\(^{-3}\)). See Table 3 for parcel model configuration details and naming conventions. See Fig. 9 for a description of time-time plots.
Fig. 11. Reisner II Ci along hourly trajectories: $N_{\text{ice}}$ generated by the Reisner II microphysical scheme in MM5 D4km are plotted along trajectories ending 12 km above Lamont. White indicates no cloud was present (IWC <0.01 mg m$^{-3}$). See Fig. 9 for a description of time-time plots.
Fig. 12. Influence of MM5 domain resolution and IN parameterization on parcel model $P(\sigma)$ and $P(N_{\text{ice}})$. $P(\sigma)$ and $P(N_{\text{ice}})$ were calculated along trajectories ending 12 km above Lamont from 12:00 to 24:00 UTC. The cloud fraction (cf) is listed after the parcel model experiment name. Cloudy air must have an IWC greater than 0.01 mg m$^{-3}$. $P(N_{\text{ice}})$ were calculated for $N_{\text{ice}}$ >0.001 cm$^{-3}$. $P(\sigma)$ were calculated for $\sigma$ >0.1. See Table 3 for parcel model experiment details and naming conventions.
Fig. 13. Model humidity and temperature 12 km above Lamont: Both the parcel model (PM_D4km, solid lines) and the Reisner II scheme (ReisnerII_D4km, dotted lines) air at Ci levels above Lamont was sub-saturated with respect to ice.