Polarized XRF Spectrometer with a 40-mW X-Ray Tube

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Submitted 30 March 2018, received in revised form 08 June 2018

A three-dimensional polarized X-ray fluorescence (XRF) spectrometer was assembled with a low-power X-ray tube of 40 milliwatts, and a sample of stainless steel was measured with an acrylic polarizer. Based on the Schrödinger’s wave picture of Compton scattering, the dependence of the de Broglie wavelength and the scattering angle of a recoil electron on the incident X-ray energy were calculated. When the incident X-rays were scattered at an angle of 90°, the de Broglie of the recoil electron always went away at an angle of 45° with the incident X-rays and the de Broglie wavelength varied for any wavelength of the incident X-rays, i.e. we could select the scattering angle of the recoil electron to be 45° according to the incident X-ray energy and it could then be regarded as 45° Bragg diffraction that could produce highly polarized X-rays. The polarization measurement of scattered X-rays from an acrylic and lead plates substantiated that Compton scattered X-rays from the acrylic plate had higher degree of polarization than the elastically scattered X-rays from the lead plate. Highly polarized Compton scattered X-rays from the light-element polarizer led to the background reduction and the changes of the characteristic X-ray intensity in XRF spectra measured by our laboratory-made spectrometer.

Key words: polarized X-ray fluorescence spectrometer, stainless steel, acrylic polarizer, Compton scattering, background.
INTRODUCTION

Polarized X-rays are produced by (i) Bragg diffraction, (ii) Barkla scattering, or (iii) the use of a secondary target [1]. When X-rays impinge on a Bragg crystal at an angle of 45°, only σ-polarization that is parallel to the crystal surface is diffracted, which leads to the perfect linear polarization. This is the Bragg diffraction method. When X-rays are scattered to a right angle (90°) with the incident direction, they are also polarized, which is called Barkla scattering [2]. When primary X-rays from an X-ray source fall on a secondary target, fluorescent X-rays are emitted from the target. The use of the secondary target with the polarized geometry is considered to be able to achieve the background reduction in XRF spectra [3].

The XRF analysis employing polarized X-rays produced by 45° Bragg diffraction was first reported by Champion and Whitting [4], where the topaz single crystal was used as a polarizer with a Philips PW 1520 wavelength dispersive spectrometer. Champion and Whitting stated, “It is not too difficult with the Philips PW 1520 instruments to rotate the X-ray tube and sample holder about the axis of the collimator.” This experiment was done before the era of solid state silicon X-ray detector. After this experiment, Young et al. [5] reported a polarized XRF analysis using Barkla scattering with an energy dispersive X-ray detector though the details are not well known because the report of Young et al. was only the conference abstract, which was referred by Ryon [1]. Then, Dzubey et al. [6] and Howell et al. [7] reported the background reduction in XRF spectra using polarized X-rays produced by carbon and polyethylene scatterers respectively. Dzubey used a molybdenum anode X-ray tube at 45 kV. Howell employed a copper and silver anode tubes as X-ray sources operated at 40 kV. Ryon et al. [8, 9] developed a cylindrical polarizer made of light-element materials, e.g. B$_2$C. A plate made of B$_2$C was curved around the side of a cylinder in order to gather X-rays emitted from an anode tube. By using the cylindrical polarizer, the X-ray intensity increased, which led to the improvement of the detection limit compared with the direct excitation. Kitov [10] theoretically derived the spectral function of the scattered radiation by a B$_2$C polarizer, which elucidated the appropriate thickness of the polarizer in order to produce the highly polarized X-rays when a molybdenum anode tube was used as an X-ray source. The simulation of the scattering efficiency of Barkla scatterers was reported by Swoboda et al. [11], in which Al$_2$O$_3$ was selected as a suitable polarizer for the analysis over a wide energy range. Revenko et al. [12] experimentally compared the scattering efficiency from metallic oxide and carbide polarizers, Al$_2$O$_3$, TiB$_2$C, TiO$_2$, Y$_2$O$_3$, and applied these scatterers to the determination of several elements concentrations in rock samples. In these previous papers [5-12], light elements were employed as Barkla scatterers in terms of the background reduction and the scattering efficiency.

The Bragg diffraction polarizer at 45° is expected to produce 100 % polarization. Using the Bragg diffraction, X-rays with particular wavelength can be produced. Aiginger et al. [13] used a single copper crystal for Cu Kα X-ray monochromator as a polarizer. The single copper crystal was cut along (113) plane (2d = 2.18 Å), by which Cu Kα X-rays were diffracted at 45°. By using the polarized X-rays, elements below Z = 29 could be excited. However, when the energy of monochromatic incident X-rays is less than absorption edges of elements in a sample, the polarized X-rays generated by the Bragg diffraction cannot excite such elements i.e. the polarization produced by the Bragg diffraction is not suited for the analysis of multiple unknown elements. The polarization by the means of X-ray scattering with light elements or various kinds of secondary targets can excite X-ray fluorescence without the limitation of the incident X-ray energy. Commercially available 3D-polarized XRF spectrometers appeared as Ametek Spectro XEPOS in 1999, Panalytical Epsilon 5 in 2003, and Rigaku NEXCG in 2008. These commercial spectrometers employ the secondary target method. In the case of Epsilon 5, for instance, the secondary targets can be attached to the spectrometer, according to quantified elements, e.g. 15 secondary targets including Ca, Fe, Ge, Zr, Ag, Mo, BaF$_2$, Al$_2$O$_3$. The applied voltage to an X-ray tube can be set from 25 to 100 kV [14]. In the case of using secondary targets, however, the polarization is far from perfect, which sometimes leads to the poor background reduction compared to using the Bragg diffraction method. Especially when using L lines as an analytical line, they add complexity to the quantitative analysis in the polarized XRF [15].

Recently, Guerra et al. [16] and Pessanha et al. [17] reported a 50 W X-ray tube 3D-polarized XRF spectrometer. Encouraged by these low power polarized XRF spectrometers, we have assembled a polarized XRF spectrometer employing an acrylic polarizer as Barkla scatterer with a low-power X-ray tube which was operated with 25 and 40 mW. Measured spectra of the stainless steel showed the decrease of the nickel Kα line (7.5 keV) compared with those measured in a non-
polarized geometry, though the measurement time set as the iron Kα peak maximum had the same intensity in both geometries. When the applied voltage was lower, the relative intensity of the continuum background originating from Bremsstrahlung and the tungsten Lβ peak (9.7 keV) was reduced in the 3D geometry. These spectral changes of the Ni K line and the continuum background in the polarized geometry were investigated based on the Schrödinger’s wave picture of Compton scattering and the polarization measurements of scattered X-rays from light- and heavy-element polarizers, through which it was found that Compton scattering from the acrylic polarizer had the higher degree of polarization than elastically scattered X-rays, and this resulted in the spectral changes in measured spectra.

SPECTROMETER DESCRIPTION AND EXPERIMENTAL DETAILS

In Fig. 1, our assembled three-dimensional (3D) polarized XRF spectrometer is shown. Fig. 1(a) is the overview of the spectrometer. The spectrometer was 25 cm in length, had a width of 10 cm, and a height of 10 cm. The metallic object that had the shape of a disk was part of a polarizer holder. The drawing from CAD (computer-aided design software) is shown in Fig. 1(b). Photos of the top view and the backside of the spectrometer are also shown in Figs. 1(c) and (d). Fig. 2 shows the inside of an acrylic block around the sample holder. The X-ray tube to the scatterer distance was 10 mm, and the sample to detector distance was again 10 mm. The X-ray path was air inside the thick acrylic block. The sample was inserted from the bottom of the acrylic block. The X-rays were made incident on a polarizer at an angle of 45°, and they were again reflected on a sample at an angle of 45°. A low power X-ray tube was a Moxtek (Orem UT) Ultra-Lite Magnum, 50 kV and 4 W, with a tungsten target [18]. As a scatterer, an acrylic ((C₅H₂O₈)n) plate was used because acrylic is composed of elements with low atomic numbers and considered to have large Compton scattering cross section. The area of the acrylic plate was 80 mm², and the thickness was 30 mm. The detector was an SDD (RES-Lab, Osaka) [19]. The area of the detector was 100 mm². The silicon crystal thickness was 450 μm. The thickness of beryllium window was 8 μm. A Peltier device was cooled down to -30 °C. Peaking time was set at 6 μs at which the energy resolution had the width of 133 eV for Mn Kα line. In order to reduce X-rays directly coming from the X-ray tube and to accurately measure the W Lβ line intensity, a lead collimator that had a 2 mm diameter hole was attached to the detector window. A stainless steel SUS 316L (ASTM 316L) was measured by the polarized spectrometer. Applied voltage and current were 25 kV, 1 μA (25 mW) and 40 kV, 1 μA (40 mW). A non-polarized (2D) geometry in order to compare measured spectra with the polarized geometry is shown in Fig. 3. The angle among X-ray tube, sample, and the detector was set at 90°. The X-ray tube to the sample distance was 10 mm, and the sample to detector distance was also 10 mm. White arrows depicted in Fig. 3 indicate the X-ray path. In order to achieve the same number of counts on the Fe Kα, the dwelling time was changed according to the spectral intensity.

In order to evaluate the polarization of scattered X-rays from polarizers, a spectrometer for the polarization measurement was made. An X-ray tube, a polarizer, an analyzer, and a detector were arranged as shown in Fig. 4. The incident X-rays were first scattered on...
the polarizer at an angle of 45°, and then X-rays were again scattered in the direction of 45° with the analyzer. With the use of a 3D printer, holders were made of a polylactic resin, which could change the detection angle θ by every 30° in the y-z plane in Fig. 4(a). θ was defined as the angle between the directions of the incident X-rays and the scattered X-rays from the analyzer. The intensity of scattered X-rays was measured changing the detection angle. The X-ray tube was the same one as the above, which was operated at 25 kV and 20 μA. An acrylic and lead plates were used as polarizers, whose ratios of elastic and Compton scattering cross section were different as 1.6 : 1.0 of carbon and 33 : 1.0 of lead for 10-keV photons [20]. An acrylic plate was employed as the scattering analyzer. Polarizers and the scattering analyzer could be attached to the X-ray tube holder and the detector holder. The degree of polarization of scattered X-rays was evaluated as the ratio of an amplitude of a modulation curve to the average of scattered X-ray intensity, \( \frac{N_{//} - N_{//}}{N_{//} + N_{//}} \). Here, \( N_{//} \) and \( N_{//} \) denote the intensity of scattered X-rays when the detection angle is parallel (θ = 0° as shown in Fig. 4(c)) and perpendicular (θ = 90° as shown in Fig. 4(e)) to the direction of the incident X-rays.

**RESULTS and DISCUSSION**

Figures 5 and 6 show XRF spectra of stainless steel SUS 316L (ASTM 316L), the main components of which were Fe, Cr (16%), Ni (10%) and Mo (2%). Pb was originated from the X-ray collimator placed on the detector window. We compared spectra in the 3D geometry with those in the 2D geometry. Although the measuring time was changed in order to achieve the same number of counts on the Fe Kα, the measured spectra showed that the Ni Kα intensity decreased in the 3D geometry compared with that in the 2D geometry. This difference of Ni Kα intensity between the 2D and 3D geometries was due to Compton scattering. The W Lα energy is 8.396 keV, and the Ni Kα absorption edge is 8.330 keV. The difference is only 66 eV. The energy shift when the incident X-rays were Compton-scattered at an angle of 90° is 136 eV. Thus, the energy of the scattered W Lα line was shifted to the lower side, 8.260 keV, which was less than the Ni K absorption edge. The Compton scattered W Lα line could not therefore excite Ni K line. Sasaki et al. [21] reported the intensity of Compton scattering lines when measuring spectra of an acrylic plate with a rhodium target X-ray tube was much higher than that of the elastic lines. Therefore, when employing low-atomic number materials as polarizers, Compton scattering effect on spectra is not negligible.

As is found from Fig. 5 (25 kV tube potential), the relative intensity of the continuum background originating from Bremsstrahlung and the W Lβ peaks from the X-ray tube was weaker in the 3D geometry compared with that in the 2D geometry in the energy range of from 7 to 15 keV. As shown in Fig. 6, on the other hand, the continuum background and the W Lβ peaks had essentially the same intensity for both of the 3D and 2D geometries when the X-ray tube voltage was 40 kV.

In order to consider the reason why the continuum background and the W Lβ peak intensity were weaker
in the 3D geometry compared with the 2D geometry when the lower voltage was applied to the X-ray tube, Compton scattering that occurred on the acrylic polarizer should be addressed. When the incident X-ray energy is 10 keV (= ħω in Fig. 7), the Compton scattered X-ray energy by a free electron in the scatterer observed at θ = 90° is 200 eV less (= ħω - ħω'). The shifted X-ray energy by 200 eV is converted to the kinetic energy of the free electron, and thus the group velocity (u in Fig. 7) of the recoil electron is 8.2·10^6 m/s. The de Broglie wavelength (Λ in Fig. 8) of this electron can be estimated to be 0.1 nm (1 Å). The wave velocity (phase velocity, U) of the de Broglie wave is p/(2m), which is half of the group velocity p/m and thus is 4.1·10^6 m/s. Here the momentum of electron p is related to the de Broglie wavelength Λ as Λ = ħ/p. The de Broglie wave is the periodic electron density, in other words, a periodic lattice, moving with the phase velocity depicted in Fig. 8. The incident X-rays are, therefore, Bragg-diffracted by the moving periodic lattice, and thus the diffracted X-ray wavelength is Doppler-shifted to the longer wavelength, expressed by 200 eV less photon energy. The length of a wave train associated with one electron moving with a kinetic energy of 200 eV is said to be ten nanometers. The wavelength of the electron density wave can be inversely regarded as a lattice constant, and the incident X-rays are diffracted by the de Broglie wave of the recoil electron going away from the X-rays with the phase velocity of about one percent of the light speed. This is the Schrödinger’s picture of Compton scattering [22-25].

When the incident X-ray energies were 1, 10, 15, 25, and 40 keV, phase velocity, the de Broglie wavelength, and the scattering angle of the recoil electron were calculated as shown in Table. Each de Broglie wavelength of the recoil electron and phase velocity depended on the incident X-ray energies. On the other hand, the scattering angle kept almost 45°. Combined with the wave picture of Compton scattering, the de Broglie wave of the recoil electron in the polarizer can be regarded as a Bragg crystal that is moving to the direction of a particular angle, of which moving direction becomes much closer to the angle of 45° when the incident X-ray energy becomes lower. Namely, the de Broglie wave moving away from the X-rays with the phase velocity of about one percent of the light speed. This is the Schrödinger’s picture of Compton scattering [22-25].

| Incident X-ray energy (keV) | Phase velocity, U (Light speed units) | de Broglie wavelength of the recoil electron, Λ (Å) | Scattering angle, φ |
|----------------------------|--------------------------------------|--------------------------------------------------|-------------------|
| 1                          | 1.4·10^-3                            | 8.8                                              | 44.9°             |
| 10                         | 1.4·10^-2                            | 0.9                                              | 44.4°             |
| 15                         | 2.0·10^-2                            | 0.6                                              | 44.2°             |
| 25                         | 3.4·10^-2                            | 0.4                                              | 43.6°             |
| 40                         | 5.3·10^-2                            | 0.2                                              | 42.8°             |
Broglie wavelength of the recoil electron corresponds to the lattice spacing that changes itself with the incident X-ray energy so as to diffract X-rays at the angle of 45º for any wavelength of the incident X-rays. As 45º Bragg diffraction can theoretically produce the perfect polarized X-rays, polarizers made of light elements which have a large Compton scattering cross section is able to make the incident X-rays highly polarizable over a wide energy range.

In order to experimentally prove that Compton scattered X-rays were more highly polarized than elastically scattered X-rays, the degree of polarization of scattered X-rays by the acrylic and lead plates were measured. Fig. 9 shows the angular dependence of the integrated intensity of scattered X-rays in the energy range of (a) 0 to 25 keV and (b) 9.4 to 9.7 keV. Solid dots (measured) and lines (fitted) are for acryl, and broken ones are for Pb.

Estimated degrees of polarization were 0.74 and 0.58 when using the acrylic and lead plates respectively. This result of the polarization measurements showed that the acrylic polarizer composed of light elements of which Compton scattering cross section was large could produce polarized X-rays with the higher degree of polarization than the lead plate. Previous papers related to Barkla scattering polarization [5-12] employed light-element polarizers, in which the large background reduction was achieved because the inelastic Compton scattered X-rays were used as excitation sources rather than the elastic scattering.

In the present study, the $W_L^\alpha$ and $L_B^\beta$ lines from the X-ray tube were not only elastically but also inelastically scattered. The energy difference between elastic and inelastic scattering is difficult to be experimentally discriminated according to the resolution of the X-ray detector used, and we sometimes regard them as the elastically scattered characteristic lines from the X-ray tube. However, truly, the majority is the inelastic Compton scattering, especially when a polarizer made of light-element materials is employed. When using the incident X-rays with lower energy, the scattering angle of the electron becomes close to 45º. Therefore, Compton scattered X-rays from the acrylic scatterer were highly polarized when the applied voltage was 25 kV, which led to the reduction of the spectral background and the $W_L^\alpha$ lines.

CONCLUSIONS

We assembled the low-power 3D-polarized XRF spectrometer with the acrylic polarizer and compared measured spectra of the stainless steel between the 3D and 2D geometries. The measured spectra showed that the Ni $K\alpha$ intensity decreased, which was because the energy of the $W_L^\alpha$ line was Compton-shifted to the lower energy side than the Ni $K$ absorption edge. When the lower voltage was applied to the X-ray tube in the 3D geometry, the spectral background and the $W_L^\beta$ peak from the X-ray tube were reduced. Based on Schrödinger wave picture of the Compton scattering, the de Broglie wave can be regarded as Bragg crystal that changes its lattice spacing so that it always diffracts X-rays in the direction of 45º. When X-rays diffracted by 45º Bragg diffraction were observed at $\theta = 90^\circ$, they theoretically had 100% polarization. When the applied voltage to the X-ray tube was lower, the scattering angle of the recoil electron became close to 45º, which corresponded to 45º Bragg diffraction. Thus, Compton scattered X-rays from the acrylic scatterer were highly polarized. The polarization measurements of scattered X-rays showed that X-rays scattered on the acrylic plate had the high degree of polarization. We have revealed that Compton scattering from the polarizer that was made of light elements resulted in the reduction of the background and the intensity changes of characteristic X-rays in the spectra measured by using the low-power polarized XRF spectrometer.
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