C(spⁿ)–X (n = 1–3) Bond Activation by Palladium

Thomas Hansen,[a, b, c] Xiaobo Sun,[a, b] Marco Dalla Tiezza,[a] Willem-Jan van Zeist,[a] Jordi Poater,[b, d] Trevor A. Hamlin,[a] and F. M. Bickelhaupt*[a, e]

Abstract: We have studied the palladium-mediated activation of C(spⁿ)–X bonds (n = 1–3 and X = H, CH₃, Cl) in archetypal model substrates H₂C–CH₂–X, H₂C–CH–X, and H₂C–C–X by catalysts PdLₙ, with Lₙ = no ligand, Cl⁻, and (PH₃)ₙ, using relativistic density functional theory at ZORA-BLYP/TZ2P. The oxidative addition barrier decreases along this series, even though the strength of the bonds increases going from C(sp¹)–X to C(sp²)–X, to C(sp³)–X. Activation strain and matching energy decomposition analyses reveal that the decreased oxidative addition barrier going from sp¹ to sp² to sp³, originates from a reduction in the destabilizing steric (Pauli) repulsion between catalyst and substrate. This is the direct consequence of the decreasing coordination number of the carbon atom in C(spⁿ)–X, which goes from four, to three, to two along this series. The associated net stabilization of the catalyst–substrate interaction dominates the trend in strain energy which indeed becomes more destabilizing along this same series as the bond becomes stronger from C(spⁿ)–X to C(sp³)–X.

Introduction

Catalytic processes play an indispensable role in the chemist’s toolbox and can offer exceptional control over the reactivity and selectivity of chemical transformation.[1] The transition-metal-catalyzed cross-coupling reaction (Scheme 1) offers a convenient strategy to forge C–C bonds.[2] The oxidative addition step in the catalytic cycle plays an important role in the reactivity and selectivity, and several experimental and theoretical studies have found the oxidative addition step to be the rate-determining step.[3] What is currently needed is a quantitative model to rationalize the effect of the C(spⁿ)–X hybridization of the substrate on the reactivity of the oxidative addition.[4]

Thus, to unravel the effect of hybridization of C(spⁿ)–X (n = 1–3) in the bond activation process, we have computationally explored the potential energy surface (PES) of the oxidative addition reaction of C–X (H, CH₃, Cl) catalyzed by PdLₙ, i.e., PdLₙ = Pd, PdCl⁻, and Pd(PH₃)ₙ using relativistic density functional theory at ZORA-BLYP/TZ2P (Scheme 2). We have chosen to represent common motifs of reactants in transition-metal-catalyzed reactions through archetypal model R–X substrates,
with $R = H_2C-CH_2-$, $H_2C=CH-$, $HC=CH-$, $HC\equiv C-$, $X = H, CH_3, Cl; PdL_n = Pd, PdCl, Pd(PH_3)$.

**Activation strain and energy decomposition analysis**

To analyze and compare the reaction pathways of the different systems, we used the activation strain model (ASM) of chemical reactivity. This model is a fragment-based approach in which the PES can be described and understood with respect to the reactants. It takes into account the rigidity of the reactants and the amount of deformation that occurs during the reaction, as well as their inclination to interact with each other during the oxidative addition. Using this model, the total energy, $\Delta E(\zeta)$, is decomposed into the strain and interaction energy, $\Delta E_{strain}(\zeta)$ and $\Delta E_{int}(\zeta)$, respectively, and these values are then projected onto the reaction coordinate $\zeta$ as in the Eq. (1).

$$
\Delta E(\zeta) = \Delta E_{strain}(\zeta) + \Delta E_{int}(\zeta)
$$

In this equation, the energy required to deform the reactants from their equilibrium structure to the geometry they adopt during the reaction at an arbitrary point $\zeta$ of the reaction coordinate is identified by the strain energy, $\Delta E_{strain}(\zeta)$. On the other hand, the deformed reactants interact along the reaction coordinate and this contribution is entirely accounted for by the interaction energy, $\Delta E_{int}(\zeta)$.

A further decomposition of the interaction energy by means of quantitative Kohn-Sham molecular orbital (KS-MO) theory together with a canonical energy decomposition analysis (EDA) is also possible. The EDA decomposes the $\Delta E_{int}(\zeta)$ into the following three energy terms shown in Eq. (2)

$$
\Delta E_{int}(\zeta) = \Delta V_{disp}(\zeta) + \Delta E_{Pauli}(\zeta) + \Delta E_{ori}(\zeta)
$$

From this equation, the quasi-classical electrostatic potential interaction between the unperturbed charge distributions of the deformed reactants is accounted for by the $\Delta V_{disp}(\zeta)$ term. This term is usually attractive. The Pauli repulsion, $\Delta E_{Pauli}(\zeta)$, on the other hand, considers the destabilizing interaction between the occupied orbitals of both fragments and it arises from the antisymmetrization of the wavefunction. Lastly, the orbital interaction energy, $\Delta E_{ori}(\zeta)$, accounts for polarization and charge transfer (e.g., HOMO–LUMO interactions) between the fragments.

In the present paper, the activation strain and energy decomposition diagrams are plotted using the PES from the intrinsic reaction coordinate (IRC) calculation. The energy is projected onto
the bond stretch of the activated R–X bond. This is the dominant reaction coordinate for the studied oxidative addition reactions going from the reactant complex via the transition state to the product. For this reason, it is shown to be a reliable reaction coordinate for studying bond activation reactions. Consistent geometries were extracted from the IRC. To ensure that our consistent geometries were not skewed by the step size of the IRC, identical structures for all considered systems, in terms of the reaction coordinate, were obtained by linear interpolation of two adjacent IRC points.

**Thermochemistry**

The bond dissociation energies (BDE), also known as bond enthalpies (ΔH_{diss}), are calculated at normal temperature and pressure (NTP, i.e., 298.15 K and 1 atm) from electronic bond energies (ΔE) and vibrational frequencies using the canonical thermochemistry relations for an ideal gas [Eq. (3)].

\[ \Delta H_{diss} = \Delta E + \Delta E_{trans} + \Delta E_{rot} + \Delta E_{vib} \]

Herein, \( \Delta E_{trans} \), \( \Delta E_{rot} \), and \( \Delta E_{vib} \) are the differences in translational, rotational, and zero-point vibrational energy between the R–X substrate and the homolytically dissociated fragments, R' and X'. The last term, \( \Delta (\Delta E_{vib})_{trans} \), is the vibrational correction energy to bring the system from 0 K to 298.15 K.

| Table 1. C(spⁿ)–X (n = 1–3) bond lengths (in Å) and homolytic dissociation enthalpies (in kcal mol⁻¹).²⁴ |
|---------------------------------------------------------------|
| Substrate | C(spⁿ)–X (Å) | ΔH_{diss} |
| H₃C–CH₂–H | 1.098 | 97.1 |
| H₃C–CH–H | 1.089 | 106.0 |
| HCl–C–H | 1.067 | 131.1 |
| H₃C–CH₂–CH₃ | 1.541 | 79.8 |
| H₃C–CH–CH₃ | 1.508 | 92.3 |
| HCl–C–CH₃ | 1.462 | 120.7 |
| H₂C–CH₂–Cl | 1.846 | 76.9 |
| H₂C–CH–Cl | 1.764 | 87.8 |
| HCl–C–Cl | 1.652 | 106.2 |

[a] Computed at ZORA-BLYP/TZ2P (enthalpies at 298.15 K).

| Table 2. Energies relative to reactants (in kcal mol⁻¹) of the stationary points along the C(spⁿ)–X bond activation by Pd₃ model catalysts²⁴ |
|---------------------------------------------------------------|
| Activation Bond | Pd-catalyst | Substrate | Bond type | RC | TS | P |
| C–H | Pd | H₃C–CH₂–H | sp³–H | –6.7 | 4.6 | –3.7 |
| | | H₃C–CH–H | sp²–H | –33.6 | –3.5 | –7.5 |
| | | HCl–C–H | sp–H | –33.5 | –9.9 | –11.2 |
| | PdCl²⁻ | H₃C–CH₂–H | sp³–H | –12.3 | –4.2 | –7.6 |
| | | H₃C–CH–H | sp²–H | –40.6 | –16.4 | –17.2 |
| | | HCl–C–H | sp–H | –41.9 | –32.0 | –33.6 |
| | Pd(PH₃)₂ | H₃C–CH₂–H | sp³–H | [a] | 34.3 | 29.5 |
| | | H₃C–CH–H | sp²–H | [a] | 25.9 | 23.0 |
| | | HCl–C–H | sp–H | [a] | 14.1 | 10.1 |
| C–C | Pd | H₃C–CH₂–CH₃ | sp³–CH₃ | –6.8 | 20.1 | –8.2 |
| | | H₃C–CH–CH₃ | sp²–CH₃ | –31.3 | 9.9 | –8.4 |
| | | HCl–C–CH₃ | sp–CH₃ | –31.6 | 6.7 | –9.2 |
| | PdCl²⁻ | H₃C–CH₂–CH₃ | sp³–CH₃ | –12.6 | 17.1 | –8.7 |
| | | H₃C–CH–CH₃ | sp²–CH₃ | –37.9 | 1.5 | –9.5 |
| | | HCl–C–CH₃ | sp–CH₃ | –38.3 | –7.2 | –26.1 |
| | Pd(PH₃)₂ | H₃C–CH₂–CH₃ | sp³–CH₃ | [a] | 53.2 | 29.5 |
| | | H₃C–CH–CH₃ | sp²–CH₃ | [a] | 42.9 | 27.2 |
| | | HCl–C–CH₃ | sp–CH₃ | [a] | 38.9 | 18.6 |
| C–Cl | Pd | H₃C–CH₂–Cl | sp³–Cl | –13.5 | –0.9 | –32.5 |
| | | H₃C–CH–Cl | sp²–Cl | –31.8 | –15.9 | –33.3 |
| | | HCl–C–Cl | sp–Cl | –35.2 | –17.5 | –35.1 |
| | PdCl²⁻ | H₃C–CH₂–Cl | sp³–Cl | –17.8 | –6.5 | –53.1 |
| | | H₃C–CH–Cl | sp²–Cl | –45.4 | –24.4 | –55.4 |
| | | HCl–C–Cl | sp–Cl | –49.7 | –29.7 | –65.7 |
| | Pd(PH₃)₂ | H₃C–CH₂–Cl | sp³–Cl | [a] | 27.2 | –7.9 |
| | | H₃C–CH–Cl | sp²–Cl | [a] | 15.4 | –10.1 |
| | | HCl–C–Cl | sp–Cl | [a] | 12.6 | –23.6 |

[a] Electronic energies computed at ZORA-BLYP/TZ2P. [b] RC is unbound.
The bond strength of C(sp²)–X, which can be traced back to the more stabilizing C(sp³)–Cl bonds; PdCl₃, in line with earlier work on C(sp³)–X bonds.⁴⁹ Here, we find that the activation of C(sp³)–X closely follows the reactivity trends found for the sp² in H₂C=CH–X. For example, the ΔE° of the C–H bond activation of benzene and ethene is −1.4 and −3.5 kcal mol⁻¹, respectively (see Table S3).

**Activation strain analyses**

Next, we applied the activation strain model (ASM) of chemical reactivity to gain quantitative insight into the physical factors governing the bond activation process. Figure 2 shows the computed activation strain diagrams (ASDs) of the C–H activation between Pd + R–H with R = H₂C=CH– (red), H₂C=CH– (blue), and HCl– (black). All other model reactions, i.e., C–C, C–Cl bonds; PdCl₃, Pd(PH₃)₂ catalyst complexes, lead to similar ASDs with similar characteristics (see Figures S1 - S3).

In the ASM, the total energy profile (ΔE) is decomposed into the strain energy (ΔEstrain) and the interaction energy (ΔEint): ΔE = ΔEstrain + ΔEint. The strain energy originates from the deformation of the reactants along the reaction coordinate. The interaction energy accounts for all chemical interactions between the deformed reactants. As found in Table 2, the reaction barrier decreases going from C(sp²)–X > C(sp³)–X > C(sp³)–X, which can be traced back to the more stabilizing interaction energy between Pd and the substrate. The strain energy, on the other hand, gives rise to the opposite trend and becomes more destabilizing along this same series. This trend in strain energy originates from the increasingly stronger C–H...
bond (see Table 1), going from sp^3 (H,C–CH_3–H: ΔH_{fSOC} = 97.1 kcal mol^{-1}), to sp^2 (H,C–CH–H: H_{fSOC} = 106.0 kcal mol^{-1}), to sp (H,C≡C–H: ΔH_{fSOC} = 131.1 kcal mol^{-1}). However, the more significant strengthening in the stabilizing interaction energy between the catalyst and substrate along this series is able to overrule the increasingly destabilizing strain energy that goes with the activation of the relatively stronger bond. Additionally, again the data of the C(sp^3)σ-C,σ–X closely follow the reactivity trends found for the sp^2 (see Figure S4).

To understand the significantly more stabilizing interaction energy going from C(sp^3)–X to C(sp^3)–X to C(sp)–X, we apply a canonical energy decomposition analysis (EDA), in which we decompose the ΔE_{int} between the deformed reactants into three chemically intuitive energy terms, i.e., ΔE_{Pauli}, ΔV_{elstat} and ΔE_{str}. The more stabilizing interaction along C(sp^3)–X, C(sp^3)–X, and C(sp)–X appears to be mainly caused by the more stabilizing orbital interactions. Note that these EDA plots should be interpreted with caution. We previously found^{27a–c} as one would expect, that the EDA results are strongly dependent on the distance between the reactants, in this case, the catalyst and substrate. The Pd–C distance is more than 0.2 Å longer for the Pd + H,C–CH_3–H than Pd + H,C≡C–H, i.e., 2.14 Å and 1.92 Å, respectively, at the same consistent TS-like geometries (C–H bond stretch of 0.50 Å), as obtained from the IRC. The vastly different catalyst–substrate distance for C(sp^3)–X, C(sp^3)–X, and C(sp)–X is directly caused by the steric (Pauli) repulsion between the catalyst and substrate. The steric repulsion between the catalyst and substrate pushes the Pd substantially further away for H,C–CH_3–H than H,C≡C–H at the same C–H bond stretch. This effectively causes all EDA terms to be smaller in absolute magnitude for H,C–CH_3–H (i.e., a less destabilizing ΔE_{Pauli} less stabilizing ΔV_{elstat} and ΔE_{str}).

To remedy the impact of the different catalyst–substrate bond lengths on the individual EDA terms, we artificially constrained the Pd–H and Pd–C bond lengths of Pd + H,C–CH_3–H and Pd + H,C≡C–H to that of Pd + H,C≡C–H, while keeping the C–H bond stretch constant. We constructed these geometries based on the above discussed consistent TS-like geometries (C–H bond stretch of 0.50 Å) that we obtained from the IRC. As one would expect, the destabilizing steric (Pauli) repulsion significantly increases, i.e., ΔΔE_{Pauli} = +97.1 kcal mol^{-1}, as does the orbital interaction, i.e., ΔΔE_{elstat} = –27.0 kcal mol^{-1}, and electrostatic attraction, i.e., ΔΔV_{elstat} = –63.5 kcal mol^{-1} for Pd + H,C–CH_3–H.

Table 3 summarizes the data of this numerical experiment for Pd + R–H with R = H,C–CH_3–H, H,C≡C–H, H,C≡C–H. The same trends are obtained for C–C and C–Cl bond activation (see Tables S4 and S5). Table 3 shows that the catalyst–substrate interaction becomes more stabilizing going from C(sp^3)–X, to C(sp^3)–X, to C(sp)–X, in line with the ASM/EDA curves as function of the reaction coordinate in Figure 2. This trend originates from the steric (Pauli) repulsion, which becomes significantly less destabilizing along this series, i.e., 295.2, 277.1, and 245.3 kcal mol^{-1}. The less destabilizing steric (Pauli) repulsion originates from the decreasing coordination number of the carbon atom in C(sp^3)–X along this series, causing less steric interactions between closed shells on the catalyst and closed shells with amplitude on the substituents of the substrate. In parallel, the initially found more stabilizing orbital interaction along the same series is maintained in our numerical experiment, however, this trend is significantly less steep than the steric (Pauli) repulsion, going only from –112.7, to –120.3, to –129.6 kcal mol^{-1}. This can be directly traced back to the systematically lower-lying σ^*_{C–X} orbital of the substrate going from C(sp^3)–X, to C(sp^3)–X, to C(sp)–X. For example, along this series with X = H, the energy decreases from 1.2 (H,C–CH_3–H), to 0.9 (H,C–CH_3–H), to 0.5 eV (H,C≡C–H). The other substrates, i.e., C–C, C–Cl bonds also show the same behavior (see Table S6). The stabilization of the σ^*_{C–X} orbital along this series is due to a decrease of antibonding overlap of the carbon 2s atomic orbital with the decreasing number of substituent lobes and an increase in bonding overlap of the carbon 2p atomic orbital with an increasingly more favorably aligned substituent lobe going from sp^3 to sp^2 to sp, respectively.^{110} This facilitates a
stronger π-backdonation from the catalyst to the substrate. Concluding, both the enhanced orbital interaction and less destabilizing steric (Pauli) repulsion cause a lower reaction barrier following C(sp²)–X > C(sp³)–X > C(sp)–X, in which the latter one is considerably more important.

**Conclusions**

The reaction barrier for C(sp³)–X bond activation (n = 1–3) systematically decreases along the series C(sp³)–X > C(sp²)–X > C(sp)–X, as follows from our quantum chemical analyses based on relativistic DFT. This reactivity trend is found for all bond types (C–H, C–C, C–Cl) and model catalysts (Pd, PdCl₂, Pd(Ph)₂) in this work. Interestingly, we establish that the trend of decreasing reaction barriers occurs whereas, along C(sp³)–X, to C(sp²)–X, to C(sp)–X, the bonds become substantially stronger and require more energy to break during the oxidative addition step.

Our activation strain and energy decomposition analyses reveal that the decreased reaction barrier going from C(sp³)–X, to C(sp²)–X, to C(sp)–X is caused mainly by a reduction in steric (Pauli) repulsion between the catalyst and the substrate. This originates from the decreasing coordination number of the carbon atom in C(sp³)–X of the substrate going from sp³, to sp², to sp. This trend is somewhat reinforced by an increasingly stabilizing orbital interaction, which is the result of a smaller and more favorable catalyst–substrate HOMO–LUMO gap, as the orbital energy of the substrate σ* C–X orbital drops along sp³, sp² and sp (cf. Vermeeren et al.¹⁵). In contrast, the required strain energy becomes significantly more destabilizing along this same series, which originates directly from the intrinsically stronger bond strength. However, the reduction in steric (Pauli) repulsion can overcome the required intrinsic higher destabilizing strain.

In all, the higher reactivity of the studied oxidative addition reactions going from C(sp³)–X, to C(sp²)–X, to C(sp)–X is not controlled by the bond strength of the R–X bond. Instead, it originates from a relief in the steric (Pauli) repulsion found between the catalyst and the substrate. The diminished steric (Pauli) repulsion for C(sp²)–X and C(sp)–X bonds makes them an ideal substrate for transition-metal-catalyzed cross-coupling reactions.

**Supporting Information**

Additional computational results; Cartesian coordinates, energies, and the number of imaginary frequencies of all stationary points.

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**Conflict of Interest**

The authors declare no conflict of interest.

**Data Availability Statement**

The data that support the findings of this study are available in the supplementary material of this article.
Keywords: activation strain model · density functional calculations · homogeneous catalysis · oxidative addition · reactivity

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