High-energy neutrino fluxes from AGN populations inferred from X-ray surveys

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ABSTRACT
High-energy neutrinos and photons are complementary messengers, probing violent astrophysical processes and structural evolution of the Universe. X-ray and neutrino observations jointly constrain conditions in active galactic nuclei (AGN) jets: their baryonic and leptonic contents, and particle production efficiency. Testing two standard neutrino production models for local source Cen A (Koers & Tinyakov 2008; Becker & Biermann 2009), we calculate the high-energy neutrino spectra of single AGN sources and derive the flux of high-energy neutrinos expected for the current epoch. Assuming that accretion determines both X-rays and particle creation, our parametric scaling relations predict neutrino yield in various AGN classes. We derive redshift-dependent number densities of each class, from Chandra and Swift/BAT X-ray luminosity functions (Silverman et al. 2008; Ajello et al. 2009). We integrate the neutrino spectrum expected from the cumulative history of AGN (correcting for cosmological and source effects, e.g. jet orientation and beaming). Both emission scenarios yield neutrino fluxes well above limits set by IceCube (by \(4\times10^6\) at 1 PeV, depending on the assumed jet models for neutrino production). This implies that: (i) Cen A might not be a typical neutrino source as commonly assumed; (ii) both neutrino production models overestimate the efficiency; (iii) neutrino luminosity scales with accretion power differently among AGN classes and hence does not follow X-ray luminosity universally; (iv) some AGN are neutrino-quiet (e.g. below a power threshold for neutrino production); (v) neutrino and X-ray emission have different duty cycles (e.g. jets alternate between baryonic and leptonic flows); or (vi) some combination of the above.

Key words: black hole physics — neutrinos — acceleration of particles — galaxies: active — galaxies: jets — X-rays: galaxies.

1 INTRODUCTION
Astronomy has relied heavily on photon-based observations. Photons participate in electromagnetic interactions, and they inevitably suffer absorption and scattering within the emitting sources and in the media along the line of sight. Neutrinos are neutral, relativistic particles, but, unlike photons, only interact weakly with matter. As they are practically unabsorbed and unscattered over a large distance, even propagating through very dense media, they can be used to probe the physics of systems at distances as far as the edge of the observable universe. Neutrinos are therefore complementary to photons as astrophysical messenger particles.

Neutrinos can be generated in violent astrophysical environments. Active galactic nuclei (AGN) and the associated jets, together with stellar objects such as pulsars, magnetars, supernovae and \(\gamma\)-ray bursters, are identified as potential sources of high-energy neutrinos (Bednarek et al. 2007; Waxman 2007; Becker 2008). AGN are the most luminous persistent X-ray sources known. At their cores resides a massive black hole (with mass \(M_\bullet \approx 10^6 - 10^9 \, M_\odot\)), and the accretion of material into their central massive black hole powers the AGN activities. The accretion process in AGN is often accompanied by a material outflow, which manifests as relativistic jets at kpc to Mpc scales. Various scenarios for high-energy neutrino production in AGN jets have been proposed (see e.g. {\sc Mannheim} 1993; {\sc M"{u}cke} et al. 1993; {\sc Atwood} & {\sc Dermer} 2003; Koers & Tinyakov 2008; Becker & Biermann 2004). The basic mechanism can be understood as follows. Charged hadrons, such as protons, are first accelerated to very high energies inside the jet. A possi-
ble acceleration site is at shocks formed inside the jet body (e.g. Blandford & Rees 1974, Harder 1973, Begelman et al. 1984, Biermann & Strittmatter 1987). The high-energy protons accelerated by the jet interact with the ambient particles (e.g. cosmic microwave background (CMB) photons or the baryons in the environments), which generates cascades of lighter children particles and subsequent production of charged pions ($\pi^\pm$ particles). The decay of these charged pions produces the high-energy neutrinos (see e.g. Becker 2008; Arg¨ uelles et al. 2010). Another possible acceleration site is at the jet base, where accretion inflow and relativistic outflow interact. The charged hadrons, presumably protons, are accelerated in shocks near the accretion disc (Stecker et al. 1991; see also Nellen et al. 1993; Stecker & Salamon 1996). Through proton-photon ($p\gamma$) interactions with the UV and X-ray photon fields from the accretion disc, neutrinos are produced through the decay of pions.

In a theoretical perspective, neutrino production is naturally associated with cosmic rays (CR), as high-energy neutrinos are products in the decay chain of energetic particles produced by interactions between CRs and ambient material and photons. In the neutral pion decay, following the proton-proton ($pp$) and $p\gamma$ interactions, $\gamma$-ray emission is also produced at comparable energies. The remarkably detailed observed CR spectrum extends over eight orders of magnitude in energy (e.g. Dermer & Menon 2002; Kotera & Olinto 2011), following a power-law with two clear breaks, and a suppression of flux towards the highest energies compatible with the GZK effect (Greisen 1966; Zatsepin & Kuz’min 1966). The transition from a Galactic to an extragalactic origin is commonly assumed to occur around $4 \times 10^9$ GeV, considering the energetics of known Galactic sources and the non-correlation between local sources and CR events (see e.g. Becker 2003; Kotera & Olinto 2011). The highest energy CR events are therefore tracers of the acceleration processes within the sources, however due to cosmic magnetic fields, the CR particles lose directionality. The neutrinos and $\gamma$-rays produced within the sources are however not affected, and whereas $\gamma$-rays attenuate upon interaction with intergalactic media, neutrinos reach us virtually unimpeded. The CR spectrum hints that their sources might emit energetic neutrinos too. Studying neutrinos and $\gamma$-rays from these sources will enable an investigation of the accelerating region within the source itself. We take this connection a step further and relate the CR emission and its derivatives (neutrinos and $\gamma$-rays) to the accretion processes driving the AGN jet.

Since CR, neutrino and $\gamma$-ray emissions are intrinsically linked, the CR and neutrino observations are thus complementary. One may naturally consider that the neutrino power scales with the $\gamma$-ray power of the AGN sources. While this could be possible for individual sources, the reality is more complicated when deriving a scaling relation applicable to the whole AGN population collectively or to an AGN subclass population from the $\gamma$-ray observations. For instance, by assuming that 10% of the $\gamma$-ray background at the MeV energies is due to non-thermal emission from AGN, such as Seyfert galaxies, Stecker (2005) obtained a flux $\Phi_{\nu} \sim 10^{-18}$ GeV$^{-1}$ cm$^{-2}$ s$^{-1}$ sr$^{-1}$ at 100 TeV for the $\mu$-neutrinos, comparable the current flux limit of $2.06^{+0.4}_{-0.3} \times 10^{-18}$ (E$_{\nu}$/100 TeV)$^{-2.06\pm0.12}$ GeV$^{-1}$ cm$^{-2}$ s$^{-1}$ sr$^{-1}$ at the same energy set by the IceCube experiment (Aartsen et al. 2013). However, the prescription of Stecker (2005) gives a neutrino flux density higher by $\sim 1.5-5$ than the current observed limit at PeV energies (see fig. 12 in Aartsen et al. 2013). Moreover, it is unclear whether or not 10% of the diffused MeV $\gamma$-rays observed in the sky is non-thermal emission from the Seyfert AGN and their relation to the neutrino generation process. It is also uncertain whether AGN in Seyfert galaxies are neutrino sources. Since the IceCube detection of TeV to PeV neutrinos (Aartsen et al. 2013; IceCube Collaboration 2013; Aartsen et al. 2013), consistent with an extragalactic origin, several studies have attempted to pinpoint the source class of these neutrino events (see e.g. Halzen 2014). Using the photohadronic interaction channel, the neutrino flux expected in blazars has been found to agree with the IceCube events assuming X-ray and $\gamma$-ray emission is produced through the $\pi^0$-decay. Dermer et al. (2014) investigates the neutrino output by via the photohadronic channel, where the CR protons interact with internal or external radiation fields. They find that low-luminosity blazars are poor producers of neutrinos, whereas $\gamma$-ray bright flat spectrum radio quasar (FSRQ) blazars are promising candidates. In our work we explore the neutrino production efficiency in AGN populations by focusing on the common engine of the AGN power. X-ray and CR emission are both driven by the central accretion processes, and the latter will result in the emission of high-energy neutrinos.

In spite of decades of intense observational and theoretical studies, in particular in the radio and X-ray wavebands, there are still many outstanding questions regarding the dynamical and chemical properties of AGN and their jets. We are unsure how much mechanical energy is stored in a jet for given observed radio and/or X-ray luminosities (see Willott et al. 1999; Merloni & Heinz 2001; Cattaneo & Best 2009; Shabala & Godfrey 2013) and we know little about the chemical ingredients in AGN jets (see Li et al. 1992; Wardle et al. 1998; Ghisellini & Celotti 2001; Böttcher et al. 2013). In the context of neutrino production, we need first to know whether AGN jets are predominantly baryonic, leptonic, both baryonic and leptonic, or electromagnetic (i.e. Poynting flux-dominated, see Lovelace 1977; Lynden-Bell 1992; Nakamura et al. 2003). We also need to know if baryons and leptons co-exist in the jet flow and if AGN jets have alternating duty cycles of baryonic and leptonic flows, analogous to active and dormant phases in terms of X-ray and radio emission.

AGN are an inhomogeneous class of objects with diverse observational properties. For instance, they may be radio-loud (RL) or radio-quiet (RQ), and their jets may be weak and episodic, or span a large spatial scale and continuously. There is no guarantee that neutrinos are produced in the same manner across all classes of AGN and that all kinds of jets in AGN are equally efficient in neutrino emission.

In this work, we address the above issues in the neutrino output in AGN jets, with an objective to set constraints on various scenarios of neutrino production in AGN, using a multimessenger approach, which combines the information obtained from X-ray observations and neutrino experiments. We use the X-ray survey observations of AGN by Chandra (Silverman et al. 2008) and Swift (Ajello et al. 2008) and derive the populations of various AGN at different cosmologi-
eral epochs. We next apply the neutrino production models and determine the neutrino emission from individual AGN. From this, we compute the energy spectra and the flux limits of the neutrinos generated by different AGN classes and accumulated throughout the history of the Universe. We then compare the flux limits to the detection limit set by the IceCube neutrino experiment (Aartsen et al. 2014), which constrains the particle content and physical properties of AGN jets, and verifies the neutrino production models proposed for different AGN classes.

This paper is organized as follows: Section 2 discusses the argument for AGN as candidate neutrino sources and the mechanisms leading to neutrino emission in AGN environments. Section 3 describes the two hadron-channel models for neutrino production in AGN. Section 4 outlines the two X-ray surveys that we use, along with a description of the X-ray luminosity function (XLF) prescriptions and the calculations of the various AGN populations we derive from this data. Section 5 presents the high-energy neutrino spectra obtained by our calculations, and Section 6 concludes with the astrophysical implications of our results.

2 NEUTRINOS FROM AGN JETS

2.1 AGN as candidate neutrino sources

Whether a charged particle could attain a certain energy depends on the duration of its confinement within the acceleration region. The Hillas (1984) criterion, which states

\[ E_{q,\text{max}} = qB\gamma r, \]

(1)
gives an estimate for the maximum energy \( E_{q,\text{max}} \) of a particle of charge \( q \) accelerated in a region with a characteristic size \( r \) and a magnetic field \( B \). AGN have emerged as candidate neutrino sources, due to their energetic nature and ability to accelerate charged particles to energies that facilitate the production of high-energy neutrinos. Taking that their outflows are hadronic, AGN and their jets are among a handful extragalactic source types that fit the requirements (see Fig. 1), and hence are potential \( 10^{20}\text{ eV} \) neutrino sources.

AGN emit electromagnetic radiation (photons) over a broad waveband from radio, sub-mm, IR, optical, UV to X-ray and \( \gamma \)-ray. They are known as strong X-ray emitters, and many AGN are discovered by X-ray observations. In practice, compact extragalactic sources observed with a persistent X-ray luminosity above \( L_X \geq 10^{42} \text{ erg s}^{-1} \) could be safely assumed as an AGN.

We would expect variations in the neutrino production rates from various AGN classes (Table 1). Often AGN are categorized into various subtypes according to their observational properties at particular wavelengths. A common divide is luminosity in radio (e.g. Antonucci 1993), which depends on whether an AGN is bright in radio emission. It can be seen releasing its energy in two oppositely directed, highly collimated, relativistic jets, perpendicular to the accretion disc (RL AGN), or with no discernible jet structure (RQ AGN). The fraction of RL systems is about 10–20 per cent of the total AGN population (e.g. Kellermann et al. 1984; Urry & Padovani 1995), and the RL fraction is estimated to reach up to 50 per cent for quasars measured in X-rays (Della Ceca et al. 1994).

Table 1. Classification of radio-loud AGN adapted from Urry & Padovani (1995). The three classes of AGN are distinguished by inclination of the radio jet to our line of sight. RGs are at high viewing angles, and consist of low radio-luminous FR Is and higher radio-luminous FR IIs. At lower viewing angles, we find RLQs, with SSRQ to FSRQ for decreasing viewing angles. At the smallest viewing angles, where the jet is directly in our line of sight, we categorize blazars, with lower luminosity BL Lacs and higher luminosity FSRQs. The RLQs and blazars are all observed with beamed luminosities, and there exists a unification scheme across the three types (see the text).

| Type                  | RG               | RLQ               | Blazars        |
|-----------------------|------------------|-------------------|----------------|
| subclasses            | FR I             | SSRQ              | BL Lac         |
|                       | FR II            | FSRQ              | FSRQ           |
| \( L_X[^{\oplus} \text{s}^{-1}] \) | \( 10^{42} - 10^{43} \) | \( 10^{44} - 10^{45} \) | \( 10^{44} - 10^{48.5} \) |

RL systems are particularly important in the study of neutrino output in AGN. Their jets must consist of highly energetic, charged particles in order to produce their observed radio luminosities. Here, we present a brief review of the various AGN subclasses. A common classification scheme includes the orientation and brightness distribution of their jets (e.g. Barthel 1988; Urry & Padovani 1995; Tadhunter 2008). Radio galaxies (RGs) are observed when the jet has a viewing angle close to 90°. The active nucleus in these systems is fully obscured or partially obscured. RGs are generally separated into two Fanaroff-Riley (FR) types, distinguishable by the strength of their radio emission (Fanaroff & Riley 1974). FR Type I (FR I) galaxies are of lower radio luminosity. They usually show a bright jet at the centre. FR Type II (FR II) galaxies are more radio-luminous. They have relatively faint central jets, but with bright termination shocks at the tip of the jet-blown lobes.

Radio-loud quasars (RLQs) and blazars are unobscured systems in which the jets are aligned along our line of sight or close to our line of sight. Their emission is therefore relativistically beamed. Radio quasars are among the very brightest and the most distant objects that we observe. They may be separated into lobe emission dominated systems with a steep radio spectrum (SSRQ) at higher viewing angles, or core emission dominated systems with a flat radio spectrum (FSRQ) at smaller viewing angles. Thus, the subclasses of radio quasars are also distinguished by the jet orientations. If the viewing angle is very small, the jet will be directed into our line of sight. This occurs in a blazar. The fraction of blazars is no more than 5% of the total AGN population. Blazars can be categorized into the high-luminosity FSRQs and the low-luminosity BL Lacs. In the framework of the AGN unification model (Urry & Padovani 1995), these two subclasses are intrinsically considered FR type II/RLQ and FR I, respectively, where the jets are aligned in our line of sight direction.

2.2 Neutrino production in AGN jets

In the hadronic scenario, energetic protons are source particles for neutrino production. Two interaction channels are proposed for neutrino production in AGN environments: one with protons interacting with ambient photons (photons from the accretion disc, synchrotron photons emitted...
The decay branching ratios of the Delta resonance $\Delta^+$ are such that two-thirds will follow the $\pi^0$-channel, and the remaining third will produce charged pions $\pi^\pm$. The pp interaction also leads to pion production, i.e. $pp \rightarrow (\pi^0, \pi^+, \pi^-)$. Radiation fields are expected to be strong at the base of the jet. In this paper, we consider only models with pp interactions and leave those with pp interactions to a future study.

Neutral pions will decay to $\gamma$-rays ($\pi^0 \rightarrow \gamma\gamma$), however the decay of charged pions produces electrons and neutrinos,

$$\pi^+ \rightarrow \mu^+ + \nu_\mu,$$

$$\pi^- \rightarrow \mu^- + \bar{\nu}_\mu,$$

$$\rho^- \rightarrow \pi^- + \nu_\mu.$$  

High-energy CRs are also products of the interactions, as escaping neutrons could undergo $\beta$-decays ($n \rightarrow p + e^- + \bar{\nu}_e$), leading to emission of neutrinos.

For neutrinos resulting from pion decay, the ratio of neutrino flavours at source is $(\nu_e : \nu_\mu : \nu_\tau) = (1 : 2 : 0)$. Due to neutrino oscillations as they propagate through space, we expect the detected ratio at Earth as $(\nu_e : \nu_\mu : \nu_\tau) = (0 : 1 : 1)$ (e.g. Becker 2008). We follow this commonly accepted picture in our paper.

However, deviations due to energy dependences on the decay rates and the strength of the source magnetic field can lead to energy loss of muons before decay (muon damping). In this case, the source ratio is lowered to $(\nu_e : \nu_\mu : \nu_\tau) = (0 : 1 : 0)$, as the electron neutrinos from the muon decays are of much lower energy than the muon neutrinos produced through the more energetic pion decays. This gives the detected flavour distribution as $(\nu_e : \nu_\mu : \nu_\tau) = (1 : 1.8 : 1.8)$ (see Kashti & Waxman 2003; Pakvasa 2008).

3. HIGH-ENERGY NEUTRINO PRODUCTION MODELS

In this study we consider the model proposed by Koers & Tinyakov (2008) and the model proposed by Becker & Biermann (2009). In both models, $p\gamma$ interaction is the dominant source process, and follows the standard picture of flavour distribution at observation as outlined above. The primary protons are accelerated through shocks in the jet, with a power-law energy spectrum. The neutrino flux is scaled by CR events detected by the Pierre Auger Observatory (PAO), assuming that the events are of AGN origin.

3.1 The Koers & Tinyakov (KT) model

The model by Koers & Tinyakov (2008) studies the relation between diffuse and point-source neutrino emission, and uses the RG nearest to us, Cen A, as a typical source for neutrino production (Fig. 3). Cen A, which lies at a distance of about 3.4 Mpc (e.g. de Vaucouleurs 1979; Soria et al. 1996, Israel 1998; Evans et al. 2004; Harris et al. 2010), is an FR I RG. As it is so close to us, it is also a well-used target for neutrino studies, as observations can be correlated with its location. The model thus follows a model of neutrino emission from Cen A by Cocco & Hammett 2008 (CH), and it in turn based on work on a neutrino production model from extragalactic sources of hadronic origin by Mannheim 2001. Following the Hillas criterion, Cen A is a fairly good candidate for high-energy particle emission, however when accounting for energy losses, it falls within the boundary of maximum proton energy $E_{p,\text{max}} \sim 10^{18}$ eV (Revenoso et al. 2011), and is from these considerations not able to produce the highest energy particles. The energy loss calculations assume an estimate for the mass of the central black hole $M_{\bullet} = 10^6 M_\odot$, the location of the confinement and acceleration $R \sim 132 R_g$ (where $R_g = GM_{\bullet}c^{-2}$ is the gravitational radius of the central black hole), maximum proton energy $E_{p,\text{max}} = 2 \times 10^{17}$ GeV and formulae for the evolution of the bulk Lorentz factor and magnetic field along the jet given in...
High-energy neutrino fluxes from AGN

The X-ray photon intensity of Cen A is \( I_{\gamma} \), using the simplest case, where the scaling factor \( \lambda \) is 1, and the fraction of proton energy that is converted to the neutrino energy and the neutron energy respectively, and

\[
\Xi(E_\nu, E_{\nu,\text{CR},br}) = \frac{E_\nu}{\eta_{\nu,\text{CR},br}}. \tag{6}
\]

Here the ratio of the average energy of neutrinos and neutrons is expressed as \( \eta_{\nu,\text{CR},br} = (E_\nu)/(E_{\nu,\text{th}}) = 0.04 \), and the fraction of the proton energy transferred to either neutrinos or neutrons in the initial interactions is given by \( \xi_\gamma/\xi_n \approx 0.1/0.5 = 0.2 \). The UHECR flux from Cen A above the threshold energy \( E_{\nu,\text{th}} \) is \( \Phi_{\nu,\text{CenA}}(E_\nu) = 5 \times 10^{-21} \text{cm}^{-2} \text{s}^{-1} \) (Ch; Koers & Tinyakov 2008). The break in the neutrino spectrum can then be expressed in terms of the UHECR proton spectrum and the expression for ratio of average energies of neutrinos and neutrons, such that \( E_{\nu,\text{br}} = \eta_{\nu,\text{CR},br} E_{\nu,\text{br}} = 4 \times 10^6 \text{ GeV} \). Due to the neutrino mixing from source to observed ratios, the muon neutrino spectrum is one third of the full neutrino spectrum, and the flux of muon neutrinos from Cen A is

\[
\Phi_{\nu,\text{CenA}} = A^{[\text{KT}]} \left( \frac{E_\nu}{\text{GeV}} \right)^{-\alpha_p} \min \left( 1, \frac{E_\nu}{E_{\nu,\text{th}}} \right), \tag{7}
\]

with a proton power-law spectrum of index \( \alpha_p = 2.7 \), and that of the neutrino spectrum \( \alpha_\nu = 1.7 \). The normalization factor, \( A^{[\text{KT}]} \) contains the scaling through the UHECR flux and the combination of energy contribution to the neutrinos from the initial particle interactions:

\[
A^{[\text{KT}]} = \left( \frac{\alpha_p - 1}{3} \right) \left( \frac{\xi_{\nu,\text{th}}}{\xi_n} \right)^{\alpha_p - 2} \frac{E_{\nu,\text{th}}^{\alpha_p - 1}}{E_{\nu,\text{br}}^{\alpha_p - 1}} \Phi_{\nu,\text{CenA}}(E_{\nu,\text{th}}), \tag{8}
\]

We note that a cut-off of the neutrino spectrum (due to it being limited by the maximum proton energy) is not included in Koers & Tinyakov (2008), as this will occur at the far end of the spectrum. We therefore assume a cut-off at an energy of \( E_{\nu,\text{max}} = 5 \times 10^{19} \text{ eV} \), at which the highest energy UHECR event is observed.

To calculate the diffuse all-sky neutrino flux, Koers & Tinyakov (2008) use two source models; one with AGN luminosity density of no evolution and another with strong evolution (Boyle & Terlevich 1998), which lead to a diffuse flux \( \sim 200 - 5000 \) times larger than that of the Cen A flux. This implies a strong detection in either case when compared to the current experimental limit for neutrino detection in IceCube (see Fig. 2; Aartsen et al. 2014).

In this paper however, we use the Cen A neutrino spectrum as given in the Koers & Tinyakov (2008) model, and convolve with AGN population densities derived from X-ray observations. Because Cen A is a typical source in this model, we use the ratio between the neutrino and X-ray luminosities as a reference, and scale the neutrino flux for an AGN of a given X-ray luminosity by this ratio:

\[
\zeta^{\text{AGN}} = \lambda \zeta^{\text{CenA}}, \tag{9}
\]

using the simplest case, where the scaling factor \( \lambda = 1 \), and

\[
\zeta^{\text{CenA}} = \left( \frac{L_X}{L_X^{\text{CenA}}} \right)^{\text{CenA}}. \tag{10}
\]

The X-ray photon intensity of Cen A is \( I_X^{\text{CenA}} = L_X/4\pi D_L^2 = 3.47 \times 10^{-10} \text{ erg cm}^{-2} \text{ s}^{-1} \). \( D_L \) is the luminosity distance, and for a local source it is the same as the measured proper
distance. Thus for Cen A, $D_L = 3.4$ Mpc = $1.049 \times 10^{25}$ cm, and a measured (2−10 keV) X-ray luminosity $L_X^{\text{Cen A}} = 4.8 \times 10^{41}$ erg s$^{-1}$ (Evans et al. 2004). As Cen A is a local source, we calculate the single source spectrum at redshift $z = 0$. For an AGN with X-ray luminosity $L_X^{\text{AGN}}$, we scale the spectrum for a single source with the Cen A brightness such that

$$\tilde{\Phi}_{\text{KT, lin}} = \frac{L_X^{\text{AGN}}}{L_X^{\text{Cen A}}},$$

(11)

giving the AGN fluxes generally,

$$\Phi_{\nu}^{\text{AGN}} = \Phi_{\nu}^{\text{Cen A}} \tilde{\Phi}_{\text{KT, lin}}.$$

(12)

This linear scaling then reflects our expectation that a bright AGN produces a higher rate of neutrinos than a lower luminosity counterpart.

3.2 The Becker & Biermann (BB) model

We compare the KT model predictions with a second model by Becker & Biermann (2009). Similar to the KT model, the BB model considers neutrinos of hadronic origin in AGN jets, and the initial seed protons are accelerated in shocks in the jet. However, in this model the peak of neutrino emission occurs further out in the jet, at the first stable shock, a distance of $r \sim 3000 r_g$ (see Fig. 3). For an additional comparison with the KT model, we have in Fig. 1 added the location of Cen A if proton acceleration occurs at a location $r = 3000 r_g$ (not accounting energy losses).

After a comparison of photon optical depths, Becker & Biermann (2009) find that the photon field that dominates the $p\gamma$ interactions is of synchrotron jet origin, with optical depth $\tau_{p\gamma} \sim 1$ for a bulk Lorentz factor of the jet $\Gamma \sim 10$. The frequency of the photon target field is therefore taken to be $f = 1$ GHz. There are no breaks in the neutrino spectrum at these energies, as the break for the radio synchrotron photons occurs at much lower energies.

Furthermore, 29 UHECR events observed by PAO appear to correlate to AGN in the super-galactic plane. The BB model therefore considers the UHECR, and hence neutrino, emission to originate in blazars and FR I AGN. The neutrino spectrum is then normalized by the proton flux.

The muon neutrino spectrum traces the proton spectrum, and has a cut-off at energies determined by the maximum energy of the energetic protons,

$$\Phi_{\nu}^{\text{BB}} = A_{\nu}^{\text{BB}} E_{\nu}^{-\alpha_{\nu}} \exp \left( -\frac{E_{\nu}}{E_{\max}} \right).$$

(13)

The normalization $A_{\nu}^{\text{BB}}$ is defined in terms of the redshift dependency factor, $\varphi_{\nu}/\varphi_{\text{CR}}$, the ratio of the Lorentz factors, $\gamma_{\nu}$ and $\gamma_{\text{CR}}$ of the neutrino and proton (CR) emission respectively; a measure of the optical depth in the source photon field, $\tau_{p\gamma}$; the Auger threshold energy; and flux at energies larger than the minimum of the proton,
High-energy neutrino fluxes from AGN

7

In the Becker & Biermann (2009) model, neutrino emission needs to originate in blazar-type AGN to be detected, due to the beamed emission. A CR point source may on the other hand have a jet misaligned with our line of sight, as the emission cone of UHECRs is significantly larger than that of the neutrinos (see Fig. 3). The redshift dependency of the emission, Becker & Biermann (2009) use the flat spectrum radio source LF from Dunlop & Peacock (1995). The scaling model can be introduced to the neutrino emission from all jetted AGN classes, hence require a high-generosity study which is insensitive to orientation effects and obscuration of the jet component. As X-rays trace the accretion power of the AGN system, a survey in this waveband fits the purpose.

Furthermore, by choosing X-ray surveys as our AGN study, there is no need for complementary observations at different wavebands, as X-ray emission implies accretion on to a SMBH at the AGN centre. We can therefore be confident that all X-ray luminous objects observed with a X-ray luminosity above $L_X = 10^{42}$ erg s$^{-1}$ are AGN (see e.g. Treister et al. 2004).

Silverman et al. (2008) measure the hard (2-8 keV) XLF of AGN up to $z \sim 5$. The sample consists of 682 AGN in total, with 31 found at redshifts $z > 3$. They use the Chandra multi-wavelength project to detect high redshift luminous AGN ($L_X > 10^{44}$ erg s$^{-1}$), and the Chandra deep field to cover the lower luminosity range. Ajello et al. (2009) have used 3 yrs of data from the Swift/BAT survey to select a complete sample of X-ray blazars to determine the evolution of blazars in the 15-55 keV band. The sample consists

$$E_{CR,\text{min}} = m_p \gamma_{CR} \times \text{GeV},$$

$$L_{\nu}^{[\text{BB}]} = \frac{(\alpha_p - 1)}{12} \left( \frac{\nu_{\nu}}{\nu_{CR}} \right) \left( \frac{\gamma_{\nu} \gamma_{CR}}{\gamma_{CR}} \right)^{5-\alpha_p} N(\gamma > E_{CR,\text{min}}) \times T_{\gamma q} \left( \frac{m_p}{4} \right)^{\alpha - p} \left( \frac{L_{\text{PAO}}}{\nu_{\gamma q}} \right)^{\alpha - p - 1} \frac{1}{10^{-10} \text{GeV}^{-1} \text{cm}^{-2} \text{s}^{-1} \text{sr}^{-1}}$$

(14)

$$L_{\text{jet}} = \frac{E_{\text{synch}}}{10^{43} \text{erg s}^{-1}},$$

This gives a disc-jet scaling in terms of the synchrotron luminosity,

$$L_{\text{disk}}^{[\text{BB}]} \approx 3.3 \times 10^{-15} (L_{\text{disk}}^{[\text{BB}]})^{1.27} \text{erg s}^{-1}.$$
of 26 FSRQs and 12 BL Lac objects in a redshift range of $0.03 < z < 4.0$.

Both AGN population surveys show that the source density evolution of AGN depends on luminosity and epoch. The number density can therefore be derived using the XLF, assuming that the luminosity distribution of the neutrino sources are complete and as inferred by Silverman et al. (2008) and Ajello et al. (2009), and can be extrapolated to redshifts up to $z = 10$.

4.1 The X-ray luminosity function

The differential XLF of a population is a measure of the number of objects per comoving volume and unit luminosity interval, as a function of X-ray luminosity and redshift, 

$$ \frac{d\Psi(L_X, z)}{d \log L_X} = \frac{d^2 N(L_X, z)}{dV d \log L_X}. $$

The present-day XLF can be expressed as a simple power-law (Ajello et al. 2009),

$$ \frac{d\Psi(L_X, z = 0)}{d \log L_X} = A \left( \frac{L_X}{L_*} \right)^{-\frac{1}{p} - 2}, $$

however, observationally there is a break, and with a high enough source count, this break can be seen. A double power-law (e.g. Ueda et al. 2003) can fit the observational data, with the faint and bright end slopes dictated by $\Gamma_1$ and $\Gamma_2$, respectively, for luminosities below and above the break luminosity $L_*$, such that

$$ \frac{d\Psi(L_X, z = 0)}{d \log L_X} = A \left( \frac{L_X}{L_*} \right)^{-\Gamma_1} + \left( \frac{L_X}{L_*} \right)^{-\Gamma_2}^{-1}. $$

The evolution of the XLF depends on the chosen model that fits the observations best. The base models are the pure luminosity evolution (PLE) and the pure density evolution (PDE), however these are not found to represent the observational data well. Therefore, modified versions of these models are used, either extending the form of the luminosity or density evolution, or formulating a combination of the two (see e.g. Ueda et al. 2003; Aird et al. 2016).

The blazar population is found to be best described in terms of a modified pure luminosity evolution (MPLE) model (Ajello et al. 2009) on a double power-law present-day XLF (Equation 20), where the evolution factor is a power law with two free parameters, $v_1$ and $v_2$, giving a general behaviour with respect to redshift, of a form first given in Wall et al. (2008),

$$ \frac{d\Psi(L_X, z)}{d \log L_X} = \frac{d\Psi[L_X/e(z), 0]}{d \log L_X}, $$

and

$$ e(z) = (1 + z)^{v_1 + v_2 z}. $$
High-energy neutrino fluxes from AGN

Table 2. Fitted XLF model parameters. Summary of the fitted parameters for each best-fitting XLF model, as given in the relevant papers: model with first letter S refers to model from Silverman et al. (2008), models with first letter A refers to the models given in Ajello et al. (2009). LLDE: luminosity dependent density evolution; MPLE: modified pure luminosity evolution, and PLE refers to the pure luminosity evolution. In brackets are the source population modelled, such that Type I/IIIs are described by an LLDE model (model B in Silverman et al. 2008), blazars and FSRQs by MPLE models (best-fitting models 7 and 10, respectively; Ajello et al. 2009), and BL Lacs by the PLE (best-fitting model 11).

| Model          | $z = 0$ Parameters | evolution parameters |
|----------------|--------------------|----------------------|
|                | ($A, \log L_\odot$) | ($L_{\odot}$, $\log L_{\odot}$) | ($\bar{L}_1$) | ($\bar{y}_1$, $\bar{y}_2$) | ($\bar{L}_1$, $\bar{y}_2$) | ($\log L_\odot$) | ($\alpha$) |
| SLDDE (Type I/II) | $-6.077^a$ | $44.33$ | $2.15$ | $1.10$ | $4.00$ | $-1.5$ | $1.9$ | $44.6$ | $0.317$ |
| AMPLE (Blazar)   | $1.379 \times 10^{-7}$ | $1.81^b$ | $-0.87$ | $2.73$ | $3.45^c$ | $-0.25^c$ | $-$ | $-$ | $-$ |
| AMPLE (FSRQ)     | $0.175 \times 10^{-7}$ | $2.42^d$ | $< -50.0^d$ | $2.49$ | $3.67^e$ | $-0.30^e$ | $-$ | $-$ | $-$ |
| APLE (BL Lac)    | $0.830 \times 10^{-7}$ | $1.0^f$ | $-2.61^d$ | $0.79^e$ | $-$ | $-$ | $-$ | $-$ | $-$ |

Notes. aThe value represents the lognormal normalisation constant, $A$, as is given in Silverman et al. (2008). bThe value represents the unlogged value of the break luminosity, $L_\odot$, where the luminosities are all normalised to $L_{44} = 10^{44}$ erg s$^{-1}$. cIn these calculations we used $\gamma_1 = -50.0$ (see Ajello et al. 2009). dThe BL Lac XLF model uses the single power law expression (Equation 23), with index $\gamma_2$. eThe blazar, FSRQ and BL Lac XLFs assume an evolution defined by the indices $\gamma_1$ and $\gamma_2$.

dominated cosmology, is measured (Peacock 2007) as

$$\frac{dV_c}{dz} = 16\pi \left( \frac{c}{H_0} \right)^3 \Omega_z \Omega (1 + z)^2 \Omega (1 + z) \Omega (1 + z), \quad (32)$$

and we use the cosmological prescriptions given in the relevant papers to maintain consistency of population ($H_0 = 70$ km s$^{-1}$ Mpc$^{-1}$, $\Omega_M = 0.7$, $\Omega_M = 0.3$). The X-ray luminosities are normalized to $L_{44} = 10^{44}$ erg s$^{-1}$ in our calculations.

As an aside, it is worth emphasizing that our calculations are conservatively based only on the well-understood AGN populations. A surprising new radio AGN class ‘FR 0’ was recognized recently: their radio cores resemble FR I cores, lacking extended radio emission (Baldi & Capetti 2013). Why the FR 0 cores fail to drill their jets farther out is unclear – perhaps due to youth, intermittency, interstellar medium obstruction (like GPS/CSS sources; e.g. O’Dea 1998; Saxton et al. 2007), or intrinsically low $\Gamma$ or slow SMBH spin (Baldi et al. 2013). Whatever the reason, if FR 0 cores turn out to be as $\nu$-bright as FR I cores, then their addition would strengthen our constraints on overall AGN neutrino production. The limits also tighten in a similar manner if, for instance, our $L_X$ cut-off has underestimated a significant contribution from lower luminosity FR I RGs (e.g. Balmaverde et al. 2006; Hardcastle et al. 2008; Capetti & Raiter 2013).

4.2 AGN number density distribution

We compute the evolutionary tracks and luminosity distributions over several cosmological epochs for all four AGN subpopulations, integrating the XLFs with respect to luminosity and redshift, respectively. To obtain estimates for the full AGN population, we scale the XLF by a correction factor $\Theta_{CF}$ to obtain the number of all AGN within our redshift range. For the RG sample we account for those obscured or too faint following Zinn et al. (2011), and assume that observed sources are 10% of the total population. However, the Silverman et al. (2008) survey collects both RL and RQ sources, so we assume the RG population accounts for 10% of all X-ray detected AGN (Urry & Padovani 1993). The correction factor for RGs is therefore $\Theta_{CF} = 1$. In the case of blazars we correct for misaligned sources, obtaining the correction factor as the ratio of the solid angle of a full sphere to the solid angle of the jet projection on to this sphere. The viewing angle is $\omega = \omega_{1/2}$, so that a jet with an opening angle of $2\omega_{1/2}$ will be not be in our line of sight if the viewing angle is larger than the half opening angle. Assuming a modest bulk Lorentz factor $\Gamma = 10$, which relates to the half opening angle by $\omega_{1/2}/\Gamma = 5$:7, these misaligned sources imply that

$$\Theta_{CF} = \frac{4\pi}{\Omega} = \frac{4\pi}{2\pi(1 - \cos(\omega_{1/2}))} \approx \frac{4\pi}{2\pi(\omega_{1/2}^2/2)} = 4\Gamma^2. \quad (33)$$

This gives a correction factor of 400, which agrees with estimates of a few hundred, or $2\Gamma^2$ (Ajello et al. 2009; Ghisellini et al. 2010; Volonteri et al. 2011). We calculate the AGN number density evolution over cosmological epochs by integrating the XLF into bins of X-ray luminosity to give the redshift distribution, such that

$$\frac{dN(z)}{dz} = \Theta_{CF} \int_{\log L_1}^{\log L_2} \Psi(L_X, z) \frac{dV_c}{dz} \frac{dL_X}{dL_X} \frac{d\log L_X}{dz}. \quad (34)$$

The luminosity dependence of the AGN population found in the XLF prescriptions motivates a closer look at the luminosity distribution of AGN in bins of redshift. We assess how the dominant luminosity class varies with redshift by integrating the XLFs over several cosmological epochs in the range of X-ray luminosity adopted in our calculations, which gives

$$\frac{dN(\log L_X)}{d \log L_X} = \Theta_{CF} \int_{\log L_1}^{\log L_2} \frac{d\Psi(L_X, z)}{dz} \frac{dV_c}{dz} \frac{d\log L_X}{dz}. \quad (35)$$

We use the appropriate luminosity range, with each bin spanning an equal size for a consistent comparison. We choose the upper and lower bounds by evaluating the maximum luminosity of an AGN, according to the Eddington luminosity of a given SMBH mass. For AGN, we assume an upper mass of $M_* \sim 10^9 M_\odot$, and we find that the maximum luminosity should be about $10^{47}$ erg s$^{-1}$. Thus for
Table 3. AGN space densities. The space densities calculated for the various AGN populations considered in a redshift range $0 < z < 10$ are shown. The luminosity ranges assumed for each population are summarised together with the corresponding unbeamed luminosity. For the blazar population we determined this intrinsic luminosity to avoid contamination from other beamed luminous sources at high redshift (see the text).

|       | RG       | Blazars | FSRQ (FR II) | BL Lac (FR I) |
|-------|----------|---------|--------------|---------------|
| $L_X$ [erg s$^{-1}$]: | $10^{42}$-$10^{47}$ | $10^{44}$-$10^{48.5}$ | $10^{46}$-$10^{48.5}$ | $10^{44.5}$-$10^{48.5}$ |
| $L_X$ [erg s$^{-1}$]: | - | $10^{40}$-$10^{44.5}$ | $10^{43.5}$-$10^{48.5}$ | $10^{49}$-$10^{44}$ |
| Space density [Mpc$^{-3}$]: | ~ $1.36 \times 10^{-4}$ | ~ $2.26 \times 10^{-4}$ | ~ $6.84 \times 10^{-6}$ | ~ $5.79 \times 10^{-4}$ |

The RL derived AGN population, our range follows that of Silverman et al. (2009), spanning six orders of magnitude.

In the case of blazars, we need to account for the beaming of these objects, as the quoted X-ray luminosities given in Ajello et al. (2009) are referring to observed luminosities. The jets of observed blazars are beamed in our direction, hence the X-ray luminosities we record for the sources are greatly enhanced by this phenomenon. As the blazar surveys probe the deep past of the Universe, the estimation of the population size is based on these luminosities, and we therefore make a cut at an intrinsic luminosity of $10^{40}$ erg s$^{-1}$. We will only take those above this luminosity to be actual blazar-derived population and the FSRQ-derived population, its brightest objects are found to peak in the redshift bin between 4 and 5. This peak moves towards lower luminosities in more recent epochs.

We calculate the intrinsic X-ray luminosity following Urry & Shafiel (1984), using the relation between observed $L_X$ and emitted luminosity $L_X$ for a relativistic jet,

$$L_X = \delta^2 L_X^\gamma,$$

where $\delta = [\Gamma(1 - \beta \cos(\theta))]^{-1}$ is the jet Doppler factor, $\beta$ is the velocity in terms of the speed of light, and the Lorentz factor $\Gamma = [1 - \beta^2]^{-1/2}$, and the viewing angle $\omega = \Gamma^{-1}$. The exponent $\gamma$ gives the enhancement of the luminosity, and for a blazar type in which only one jet is seen, $\gamma = 3 + \alpha$, where $\alpha$ is the spectral index. This exponent is due to relativistic aberration, whereby the emission is beamed forward due to the relativistic motions of the jet; contraction of the time interval, thus we observe more photons per unit time; and the blueshifting of photons, as there are a factor $\delta^\alpha$ more photons at the observed frequency than at the emitted frequency. It is found that the observed and intrinsic LFs have the same slope for high luminosities, however the observed LF will flatten towards lower luminosities because it is sensitive to the lower cut-off and steepness of the Lorentz factor distribution (Lister 2003).

We assume a representative value for the spectral index of sources in a given AGN population. We use, for the subsamples BL Lacs, $\alpha = 1.5$; for FSRQs, $\alpha = 0.6$; and the total blazar sample we use $\alpha = 1.0$ (see fig. 2 Ajello et al. 2009). This means that the lowest luminosity bound for the full blazar-derived population and the FSRQ-derived population is $10^{42}$ erg s$^{-1}$, and for BL Lacs a little higher, at $10^{44.5}$ erg s$^{-1}$. A further consideration is in order for the FSRQ-derived population, because the XLF for these sources collapses at lower luminosities, as seen in the FSRQ luminosity distribution in Fig. 4. We therefore make a lower cut for this population at $10^{40}$ erg s$^{-1}$. The assumed X-ray luminosity ranges for the AGN populations are summarized in Table 3. We find that the cuts we have made do not affect the total estimated numbers significantly.

The large-scale space density (between $0 < z < 10$) is derived for the various populations, given the comoving volume contained within a redshift of $z = 10$ is $V_c \approx 3.5 \times 10^{12}$ Mpc$^3$ (Wright 2006). These are summarized in Table 3 and agree with local AGN estimates from UHECR observations (see e.g. Takami et al. 2012 and references therein).

To check our results from these two AGN population estimates, we sum the contributions from either the luminosity bins or redshift bins, and find that the sums agree, giving the space densities as quoted in Table 3.

In view of neutrino output, we would thus expect a high production rate from bright quasars from the epoch of $z \sim 4$, and bright AGN at $z \sim 2$. If neutrino emission scales with the X-ray luminosity, these sources should then produce a higher rate of neutrinos than their lower luminosity counterparts. However, the fainter sources are more numerous, hence, despite a lower rate of neutrino production, the sheer
Figure 4. AGN redshift and luminosity distributions. The panels on the left are the redshift distributions of RGs, blazars, FSRQs and BL Lacs (top to bottom). The panels on the right give the corresponding luminosity distributions. The overall trend is that the brighter AGN peak at earlier times, whereas the low-luminosity AGN are abundant at lower redshifts. Furthermore, the bright quasars are seen to dominate at higher redshifts, suggesting the density evolution of the brightest AGN was exceeded by fainter AGN at a redshift of $z \sim 1$. See the text for details.
number of these sources would imply a considerable contribution at more local redshifts.

5 HIGH-ENERGY NEUTRINO SPECTRA

We make use of the neutrino production models described in Section 3, combined with the number distribution of neutrino sources from the AGN evolution models in Section 3, to calculate the expected high-energy spectra, assuming that AGN are indeed the dominant high-energy neutrino machines (and therefore ignoring other possible sources for simplicity).

We note the distributions of AGN both in luminosity and redshift, and find that by applying a luminosity scaling, we would expect to find the highest contribution of neutrinos from low-luminosity AGN at later times, as these sources are the most numerous in this epoch. Due to high-luminosity AGN dominating at earlier times (i.e. at redshifts $z > 4$), these should be prominent contributors, as their neutrino production rate should be considerably higher than in their low-luminosity counterparts.

The luminosity scaling model is a simple relation between the neutrino luminosity and the X-ray luminosity of the source. This assumes the X-rays originate in the accretion disc, as commonly attributed. Observationally, the radiative and kinetic jet power correlates linearly with the disc luminosity (Ghisellini et al. 2014). The KT neutrino output is scaled by a ratio of the AGN X-ray luminosity to that of the representative source, Cen A. The other scaling model, applied to the BB neutrino spectra, links the disc X-ray emission to the jet synchrotron emission, which ties the neutrino emission to the disc X-ray luminosity indirectly (see Section 3). Thus, a more powerful AGN would be brighter in X-rays. Similarly, a more powerful AGN will have greater potential to accelerate particles in its jet, and contributing to a higher rate of interactions. This again leads to an expected higher rate of neutrino production in these jets. We can therefore link the X-ray luminosity of the AGN (i.e. a direct measure of the accretion power of the AGN disc) to the neutrino luminosity (a consequence of the available energy in the AGN jet to accelerate and accommodate particle interactions of energies related to the AGN power).

We produce a single source neutrino spectrum, following the published models outlined in Section 3, and convolve this with the AGN data to obtain emission from the entire populations. We scale with luminosity to reflect the influence that the source power has on the rate of neutrino production. We also correct for cosmological effects. The neutrino flux spectrum is required in terms of observable emission on Earth, and we calculate our spectra in the source frame.

Hence, we shift our single source to different cosmological epochs, such that the emitted energy at source, $E_{\text{int}}$, is related to the energy as we would observe it on Earth, $E_{\text{obs}}$ through

$$E_{\text{int}} = E_{\text{obs}}(1 + z) .$$

We carry out the spectral calculations, and relate the intensity received on Earth, $I_{\text{obs}}$, to the intensity calculated at source, $I_{\text{int}}$,

$$I_{\text{obs}} = I_{\text{int}}(1 + z)^{-4} ,$$

to obtain the neutrino flux expected to be observed on Earth, taking into account cosmological effects such as redshift distortions. For a typical source, the intensity of the neutrino emission drops significantly with increasing redshifts, and a break in the spectrum will move to lower energies (as demonstrated in the KT model calculations). We obtain the neutrino spectra produced in AGN populations from various cosmological epochs by

$$E_{\nu}^{2}d\Phi_{\nu}^{[\text{model}]} = E_{\nu}^{2}d\Phi_{\nu}^{\text{AGN}} \frac{dN(z)}{dz} \Delta z ,$$

and produced by AGN of certain luminosities by

$$E_{\nu}^{2}d\Phi_{\nu}^{[\text{model}]} = E_{\nu}^{2}d\Phi_{\nu}^{\text{AGN}} \frac{dN(\log L_{X})}{d\log L_{X}} \Delta[\log L_{X}] .$$

The sum of the binned contributions in each case gives the total diffuse emission as we would observe it. We measure the spectra against the experimental flux limit set by IceCube,

$$E_{\nu}^{2}d\Phi_{\nu} [\text{GeV cm}^{-2} \text{s}^{-1} \text{sr}^{-1}] \leq 1.44 \times 10^{-8} ,$$

in the energy range $3.45 \times 10^{4} < E_{\nu}[\text{GeV}] < 3.66 \times 10^{7}$, determined with 1 yr of data (Aartsen et al. 2014). This is an estimate of the minimum neutrino flux required for detection, and therefore gives an upper bound on the neutrino flux, as IceCube has detected only a few tens of events so far (Aartsen et al. 2013, IceCube Collaboration 2013).

5.1 Resultant neutrino spectra

We present a representation of observable neutrino emissions originating in various cosmological epochs, or from a range of source luminosities.

5.1.1 KT model spectra

The resultant energy spectra expected from the KT model prescription is shown in Fig. 4 as the sum of contributions binned in source luminosity (solid line) or redshift (dashed line). The neutrino emission from RGs far exceeds the IceCube limit, with the dominant emission coming from local sources, $z < 1$. At lower neutrino energies ($E_{\nu} < 10^{6} \text{ GeV}$) the greatest contribution coincides with the peak of the AGN population, i.e. $1 < z < 2$.

The source luminosities dominating the neutrino emission are between $43.0 < \log L_{X} < 45.0$. Low-luminosity sources contribute comparably, due to their abundance in the near Universe. The brightest sources are few, and thus only contribute significantly at lower redshifts, due to propagation effects.

The energy spectra of neutrinos originating in the blazar and FSRQ populations also exceed the IceCube limit. The dominant epoch is $2 < z < 4$, which coincides with the peak activity of these sources. At the highest neutrino energies the local epoch dominates, and the dominant contribution at lower neutrino energies extends up to a redshift $z < 6$. The low-energy trend is stronger in the spectra with FSRQ origin than that of the full blazar population, and occurs at energies $E_{\nu} < 10^{6} \text{ GeV}$.

The luminosities of the blazar sources responsible for the majority of the neutrino emission are $45.5 < \log L_{X} < 46.5$. The lower luminosity for the FSRQ population is $\log L_{X} = 46.0$, and the neutrino contribution decreases with
Figure 5. Predicted observed neutrino emission from various AGN source populations, total diffuse emission from contributions binned in redshift (solid line) and luminosity (dotted line). The horizontal solid line is the IceCube 1-yr (IC-59) neutrino detection limit [Aartsen et al. 2014]. The neutrino emission expected from the RG population (red lines) gives the highest detection, followed by emission from blazar-derived sources (green lines) and FSRQ-derived sources (blue lines). The emission from the BL Lac derived population is the only source we cannot definitively exclude within this model. The dash-dotted line corresponds to the IceCube best-fitting diffuse neutrino spectrum [Aartsen et al. 2017], where \( \Phi_{\nu} = 2.06 \times 10^{-18} \left( E_{\nu}/(10^{5} \text{ GeV}) \right)^{-2.46} \text{ GeV}^{-1} \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1} \).

5.1.2 BB model spectra

The resultant energy spectra from the BB model prescription is shown in Fig. 5 for the two scaling models used. The sum of contributions binned in source luminosity (solid line) or redshift (dashed line) are in agreement, and the resultant spectra from the two scaling models emphasize the importance of the luminosity scaling. The neutrino spectra from the BB2 model are two orders of magnitude greater than those from the BB1 model. Overall, the BB model prescription produces lower expected total diffuse neutrino emission than that of the KT model.

The RG population is seen to again greatly exceed the IceCube limit. The dominant contribution is from local sources, decreasing with increasing redshift, and the bulk of the emission originates in bright AGN, with luminosities \( 44.0 < \log L_X < 46.0 \). Both scaling models agree on that behaviour, however the BB1 model favours the brightest AGN over the low-luminosity sources, whereas this trend is weaker in the BB2 model.

The effect of the luminosity scaling is significant for the neutrino emissions of blazars. The neutrino flux from blazars falls below the IceCube limit using the BB1 scaling, with the dominant contribution from AGN with \( 45.5 < \log L_X < 47.0 \). The BB2 scaling, however, finds comparable contributions from lower luminosity sources \( 44.0 < \log L_X < 45.5 \) and brighter sources \( 46.5 < \log L_X < 47.0 \), and the total diffuse emission exceeds the IceCube limit by about two orders of magnitude.

The epoch enclosing the peak activity of blazars and FSRQs results in the majority of the diffuse neutrino flux in these sources, \( 2 < z < 4 \). As the FSRQs are already assumed to be the upper end of the blazar luminosities, the neutrino emission decreases with increasing FSRQ luminosity. However, the flux from the epoch of \( 4 < z < 6 \) is slightly higher relative to the blazar population, due to the lower luminosities tend towards lower redshifts, and are therefore not found in the FSRQ population.

The neutrino spectra from the BL Lac population reflect the source evolution, similarly to the KT model spectra. As the population evolves negatively with redshift, the dominant neutrino contribution originates at the lowest source luminosity, and in the most local sources. The BL Lacs are the only population to be accepted as a possible neutrino producing source within the model prescriptions considered above.

6 SUMMARY AND CONCLUSION

We have calculated the XLF, and derived the total numbers, for RL AGN and blazars in different luminosity and redshift ranges. These AGN demographics are then convolved with the neutrino production model to obtain the muon neutrino energy spectra as detected on Earth. It is apparent that the neutrino emission received from the epoch of AGN peak activity is enhanced, which is a consequence of the X-ray luminosity scaling. Additionally, the importance of the luminosity scaling model is highlighted by our results (Fig. 5).

We test a number of assumptions in these calculations. The AGN source distributions are assumed to derive from complete surveys, and the evolution is correctly represented by the XLFs [Silverman et al. 2008; Ajello et al. 2009]. This gives us a fair estimate of the AGN populations at different redshifts, and correct proportions over the range of X-ray luminosities.

The modest bulk Lorentz factor, \( \Gamma = 10 \) is assumed typical for all AGN. It provides a correction factor for blazars accounting for misaligned sources, \( \Theta_{\text{CP}} = 400 \), which agrees with estimates in literature (e.g. [Rachen & Mészáros 1998]). It also determines the beaming to intrinsic source luminos-
I. B. Jacobsen et al.

Figure 6. Predicted observed neutrino emission from various AGN source populations, total diffuse emission from contributions binned in redshift (solid line) and luminosity (dotted line). The horizontal solid line is the IceCube 1-yr (IC-59) neutrino detection limit (Aartsen et al. 2014). The neutrino emission expected from the RG population (red lines) gives the highest detection, followed by emission from blazar-derived sources (green lines) and FSRQ-derived sources (blue lines). The left panel uses the luminosity scaling BB1, which leads to the acceptance of all blazars as candidate neutrino sources. The BB2 model excludes all but the BL Lac population. The dash dotted line corresponds to the IceCube best-fit diffuse neutrino spectrum (Aartsen et al. 2015), where $\Phi_{\nu} = 2.06 \times 10^{-18} [E_{\nu}/(10^5 \text{ GeV})]^{-2.46} \text{ GeV}^{-1} \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$.

The modelling of neutrino production in AGN jets relies on the knowledge of particle interaction channels, and the branching ratios of the interaction. The production site is assumed to be at the base of the AGN jet as the environment in the vicinity of the black hole core is sufficiently energetic for high-energy particle interactions to occur. Models of high-energy neutrino output from AGN lobes, the torus or intergalactic media, due to pp or $p\gamma$ interactions are also worth studying (e.g. Becker & Biermann 2009, and references therein).

The resultant diffuse neutrino fluxes predicted using these models exceed the observational flux limit set by Aartsen et al. (2014), implying the following:

(i) Cen A might not be a typical neutrino source as commonly assumed. If Cen A is an exceptionally efficient neutrino machine (Koers & Tinyakov 2008), the scaling of the neutrino yield will lead to an overestimated neutrino flux, similar to what our calculations show (Figure 5).

(ii) The two neutrino flux models we considered have overestimated the neutrino production efficiency. The KT and BB models are motivated by an observed correlation between the jet synchrotron and total power (Falcke et al. 1996; Becker et al. 2008, and references therein), and the jet-disc symbiosis model (Falcke & Biermann 1995), which therefore enables a relation between neutrino emission in the jet to the X-ray disc luminosity.

The effect of the luminosity scaling model used in each case is shown to be crucial for the estimated neutrino spectra (Figs. 5 and 6). We use a model that will favour neutrino emission from bright sources, and suppress emission from the abundant lower luminosity counterparts. The KT scaling model assumes a linear relation between the source X-ray luminosity and neutrino emission, and is normalized to that of Cen A, which is assumed to be a typical neutrino producing AGN. The BB1 and BB2 scaling models rely on the relation between the jet synchrotron and total power (Falcke et al. 1995; Becker et al. 2005; Cavagnolo et al. 2010), and the jet-disc symbiosis model (Falcke & Biermann 1995), which therefore enables a relation between neutrino emission in the jet to the X-ray disc luminosity.

Due to the scarcity of the BL Lacs population (Ajello et al. 2009) note that they can only fit a single power-law LF. This may reflect an unfair representation of the neutrino emission from this sub-population of blazars. Our neutrino emission calculations are only as good as the source density model, and any conclusion drawn with respect to neutrino emission from low or high luminosity AGN, may not be valid. It is therefore worth improving the survey data to lower luminosities to fill in the lower end of the LF, as well as towards higher redshifts. It would also be interesting to explore the intrinsic XLF of the blazar populations (e.g. Ajello et al. 2012, 2014).

The effect of the luminosity scaling model used in each case is shown to be crucial for the estimated neutrino spectra (Figs. 5 and 6). We use a model that will favour neutrino emission from bright sources, and suppress emission from the abundant lower luminosity counterparts. The KT scaling model assumes a linear relation between the source X-ray luminosity and neutrino emission, and is normalized to that of Cen A, which is assumed to be a typical neutrino producing AGN. The BB1 and BB2 scaling models rely on the relation between the jet synchrotron and total power (Falcke et al. 1995; Becker et al. 2005, and references therein), and the jet-disc symbiosis model (Falcke & Biermann 1995), which therefore enables a relation between neutrino emission in the jet to the X-ray disc luminosity.
The models assume a correlation between CR and neutrino emissions due to their common production path, e.g. through $p\gamma$ interactions. The KT model is based on the observation of UHECR emission originating in the vicinity of Cen A, however Lemoine & Waxman (2009) discuss the possibility of an accidental correlation between Cen A and the observed UHECR events.

(iii) Neutrino luminosity does not universally scale with the accretion power for all AGN subclasses, and hence not with their X-ray luminosity. This will require a more complex class dependence scaling prescription than the simple universal scaling that we have used here. The three scaling models we use are linear (KT) or power laws (BB1, BB2). The steepest scaling is given by the BB1 model, and is seen to suppress the contribution from the abundant lowest luminosity sources. As these sources are predominantly found in the nearby Universe, a suppression will then enhance the neutrino contribution from the epoch coinciding with the peak activity of bright AGN, at redshifts $2 < z < 4$.

(iv) Some AGN are not neutrino sources. For instance, there could be a power threshold only above which charged particles could be accelerated efficiently and neutrino production could occur. The low-luminosity FR Is may not be sufficiently powerful for the acceleration of particles to energies of $10^{20}$ eV (Lemoine & Waxman 2009). If FR Is are the parent population of BL Lac sources, then this would also apply to this blazar subclass. Energy loss calculations of the Cen A jet (Reynoso et al. 2011) find that Cen A is unable to obtain a proton energy exceeding $E_{p,max} \sim 10^7$ GeV. This is supported by indications of lower Lorentz factors in FR IIs than FR IIs (Dermer et al. 2013). If FR IIs are the parent population of FSRQs, then a neutrino correlation with CRs may be weak or negligible, as FR IIs are unfavoured as UHECR producers (Kotera et al. 2010). A highly efficient jet environment could lead to the UHECR population decaying before escaping the confinement, hence only neutrinos would be observable.

(v) Neutrino generation and X-ray emission have different duty cycles. Jets may have alternating duty cycle of baryonic and lepton flows, or neutrino production could occur only during some fraction of the entire X-ray lifetime of the AGN.

(vi) It is a combination of some of the above.

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