Theoretical Modeling of Emission-Line galaxies: New Classification Parameters for Mid-Infrared and Optical Spectroscopy

M. Meléndez, 1*T. M. Heckman, 1 M. Martínez-Paredes, 2 S. B. Kraemer 3 and C. Mendoza 4
1 Department of Physics and Astronomy, Johns Hopkins University, Baltimore, MD, 21218, USA
2 Instituto Nacional de Astrofísica, Óptica y Electrónica, Puebla, 72840, Mexico
3 Department of Physics, The Catholic University of America, Washington, DC 20064, USA
4 Centro de Física, IVIC, PO Box 20632, Caracas 1020A, Venezuela

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ABSTRACT
We have carried out extensive and detailed photoionization modeling to successfully constrain the locations of different emission-line galaxies in optical and mid-infrared diagnostic diagrams. Our model grids cover a wide range in parameter space for the active galaxy continuum and starburst galaxies with different stellar population laws and metallicities. We compare the predicted AGN and star-formation mid-infrared line ratios [Ne III]15.56 µm/[Ne II]12.81 µm and [O IV]25.89 µm/[Ne III]15.56 µm to the observed values, and find that the best fit for the AGN is via a two-zone approximation. This two-zone approximation is a combination of a matter-bounded component, where [Ne III] and [O IV] are emitted efficiently, and a radiation-bounded component that maximizes [Ne II] emission. We overlay the predictions from this two-zone approximation onto the optical [O III]5007/Hβ and [N II]6583/Hα diagnostic diagram derived from the Sloan Digital Sky Survey, to find that the high-density and low-ionization radiation-bounded component in our two-zone AGN approximation model provides a good lower limit for [N II] emission. This establishes a new theoretical demarcation line for the minimum AGN contribution in this diagram. This new classification results by a factor of ∼1.4 in a higher AGN population than predictions derived from previous divisions of star-forming galaxies. Similarly, we define a maximum AGN contribution in the [O III]/Hβ and [N II]/Hα diagram by using a two-zone approximation within a parameter range typical of the narrow-line region.

Key words: AGN: general – galaxies: Seyfert – Optical – IR

1 INTRODUCTION
With the advent of extensive and accurate astronomical surveys in the last few years, there has been a rapid increase of astronomical data that facilitates large-scale statistical studies. For example, the Sloan Digital Sky Survey (SDSS) contains more than 2 million optical spectra of galaxies and quasars and a few hundred thousand optical and infrared stellar spectra [Ahn et al. 2014]. Given this extraordinary amount of observations, it is clear that efficient procedures must be devised to separate and classify the different objects that populate these surveys. An approach is to classify the sources in terms of the principal excitation mechanisms of the line emitting gas. Historically, the most common line discriminant in the optical among the excitation mechanisms is the combination of the [O III]5007/Hβ and [N II]6583/Hα ratios (e.g., Baldwin et al. 1981, Veilleux & Osterbrock 1987). These ratios can separate photoionization by active star formation (hot stars) from that by the "non-thermal" power-law continuum of an active galactic nucleus (AGN). These demarcation lines can be defined empirically (e.g., Kauffmann et al. 2003, hereafter Ka03) or via photoionization modeling of the emission-line spectra (e.g., Kewley et al. 2001, hereafter Ke01). A further separation can be performed between Seyfert galaxies and low-ionization emission-line regions (Kewley et al. 2006). However, despite their great success, the identification of the most heavily dust-obscured systems...
remains a challenge for optical diagrams (e.g., Farrah et al. 2007; Satyapal et al. 2008; Goulding & Alexander 2009; Caputi 2014).

Similar diagnostics in the mid-infrared, which rely on emission from the narrow line region (NLR, Seyfert 1 galaxies show both broad- and narrow-line emission whereas Seyfert 2 galaxies only show narrow-line emission due to orientation effects), have proven to be excellent tools to separate the different galaxy excitation mechanisms. Mid-infrared diagnostics are more suitable to study dust-enshrouded systems where the effect of dust obscuration can hamper the interpretation of traditional optical diagnostics (e.g., Meléndez et al. 2008a; Abel & Satyapal 2008; Rigby et al. 2009; Goulding & Alexander 2009; Dicken et al. 2014). In general, it is important to understand the underlying excitation mechanism in dust-obscure systems because they represent a common phase in the evolution of most galaxies, especially in the early Universe at the peak of the dusty star formation and AGN activity (e.g., Toomre & Toomre 1972; Farrah et al. 2007; Veilleux et al. 2009; Caputi 2014). Mid-infrared spectra provide access to important emission lines with a wide range of critical densities and ionization potentials that allow for a precise characterization of the physical properties and excitation mechanisms in the galaxy line-emitting regions. In this respect, low-ionization lines such as [Ne II]12.81μm, which requires an ionization energy of $E_\alpha = 21.57$ eV to be produced, are common in star forming galaxies (e.g., Ho & Kent 2007). This line is well correlated with other star-formation indicators such as polycyclic aromatic hydrocarbon (PAH) features and the far-infrared continuum (e.g., Meléndez et al. 2008a). On the other hand, high-ionization lines, e.g. $[O IV]25.89\mu m$ ($E_\alpha = 54.94$ eV) and $[Ne V]14.32\mu m$ ($E_\alpha = 97.12$ eV), are good indicators of the AGN power (e.g., Meléndez et al. 2008a; Rigby et al. 2009; Pereira-Santaella et al. 2010; Weaver et al. 2010). In addition, intermediate-ionization lines such as $[Ne III]15.56\mu m$ ($E_\alpha = 40.96$ eV) can provide a unique perspective into composite systems where the AGN coexists with active star formation in the host galaxy (e.g., Meléndez et al. 2008b; Pereira-Santaella et al. 2010; LaMassa et al. 2012).

Weaver et al. (2010) (hereafter W10) presented a mid-infrared diagnostic that utilizes the most common emission lines observed in star-forming and Seyfert galaxies. The W10 $[Ne III]/[Ne II]$ and $[O IV]/[Ne III]$ diagnostic diagram shows a clear separation between AGN, star-formation, and blue compact dwarf (BCD) and Wolf-Rayet (WR) galaxies. This diagram can be quantitatively separated into three large sectors. The majority of the hard X-ray selected AGN from the Swift Burst Alert Telescope survey (BAT AGN) are located in the upper-right region where the $[Ne III]/[Ne II]$ and $[O IV]/[Ne III]$ ratios are greater than unity; for the rest of this paper we will refer to these as AGN dominated sources. Most of the star-forming and starburst galaxies are in the lower-left region with $[Ne III]/[Ne II]$ and $[O IV]/[Ne III]$ ratios less than unity, while extreme starburst galaxies are located in the upper-left region with $[Ne III]/[Ne II] > 1$ and $[O IV]/[Ne III] < 1$. Note that the selection process for the BAT AGN depends only on the galaxy hard X-ray flux ($14-195$ keV) thus providing an unbiased sample of Compton-thin AGN. Moreover, because of its high-energy selection, the sample is also unbiased toward star formation activity in the host galaxy; therefore, sources in the BAT sample have a wide range of stellar contribution to their mid-infrared spectra. Hao et al. (2009) (hereafter H09) presented similar mid-infrared diagnostics where, again, the AGN and composite systems occupy a different branch to that from pure, extreme starburst galaxies.

Despite the capabilities of these mid-infrared diagrams for distinguishing excitation mechanisms, there are few theoretical studies that attempt to define demarcation lines between activity types in galaxies. On the other hand, there are several studies that have derived theoretical classifications for star-forming galaxies and AGN based on optical diagnostic diagrams; however, these studies have been limited to the modeling of star-forming galaxies to define the boundaries between galaxy types (e.g., Ke01, Stasińska et al. 2004). In this paper we present grids of photoionization calculations that combine the AGN and starburst galaxy contributions (assuming either a constant or an instantaneous star-formation burst) to define new theoretical demarcation lines for mid-infrared and optical diagrams. Contrary to previous studies (i.e. in the optical), our new theoretical classification for starburst and AGN is based on the minimum and maximum AGN contributions to the optical emission line spectra as predicted from photoionization models of the mid-infrared diagrams.

## 2 Theoretical Models

In order to investigate galaxy physical conditions in the mid-infrared and optical emission-line regions, we use constant density models with a hydrogen column density of $10^{21}$ cm$^{-2}$ throughout (e.g., Pereira-Santaella et al. 2010; Meléndez et al. 2011), thus including radiation- and matter-bounded models depending on the ionization state (Meléndez et al. 2011). These considerations are to ensure a common set of conditions associated with the narrow-line region (NLR) illuminated by an AGN and with a star-forming region illuminated by a stellar radiation field.

We thus generate a grid of photoionization models varying the total hydrogen number density, $n_H$, and the ionization parameter (see Osterbrock & Ferland 2006),

$$U = \frac{1}{4\pi R^2cn_H} \int_{\nu_{\text{min}}}^{\infty} \frac{L_{\nu}\nu^2}{4\pi R^2cn_H} d\nu,$$

where $R$ is the distance to the cloud, $c$ is the speed of light and $Q(H)$ is the ionizing photon flux. All of our calculations have been carried out with the CLOUDY (version 10.00) photoionization code last described by Ferland et al. (2013).

### 2.1 The Active Galactic Nuclei

We assume a broken power law to model the spectral energy distribution (SED) of an AGN, as used by Meléndez et al. (2011) and similar to that suggested for NGC 5548 and NGC 4151 (Kraemer et al. 1998, 2004). It takes the form $F_\nu \propto \nu^{-\alpha}$ with $\alpha = 0.5$ below $13.6$ eV, $\alpha = 1.8$ from $13.6$ eV to $1$ keV and $\alpha = 0.8$ at higher energies. For the UV-Soft X-ray slope we take the median value derived from high-ionization mid-infrared emission lines for the BAT AGN (Meléndez et al. 2011), and the oxygen, neon and nitrogen
abundances are assumed to be $-3.31$ (Allende Prieto et al. 2001), $-4.0$ (Holweger 2001) and $-4.07$ (Holweger 2001), respectively. Despite the fact that dust is likely to be mixed in with the emission-line gas in the Seyfert galaxy NLR (e.g., Kraemer & Harrington 1998; Netzer & Laor 1993), we do not include it in our AGN models because the dust-to-gas fraction is likely to vary within these regions (e.g., Kraemer et al. 1998; Groves et al. 2004b; Kraemer et al. 2004). Therefore, to reduce the number of free parameters, we have adopted dust-free models for the NLR; however, at the end of Section 4.1 we introduce dust in our final set of AGN models and discuss its effect.

### 2.2 Starburst Galaxies

Synthesis models from STARBURST99 are used to model star-forming galaxies that are optimized to reproduce the properties of galaxies with active star formation (Leitherer et al. 1999; Vázquez & Leitherer 2005; Leitherer et al. 2010). We consider two cases for the star formation law: an instantaneous star-formation burst and star formation at a continuous rate. For the single stellar population or instantaneous star-formation burst, we adopt a total star mass of $1 \times 10^6 \, M_\odot$ to be distributed out between the upper and lower cut-off masses. Star-formation rate for the continuous models is $1 \, M_\odot \, Y_\odot^{-1}$. We also adopt a double power law for the stellar initial mass function (IMF) of the type presented by Kroupa (2001). In this double Kroupa-type law there are two exponents, 1.3 and 2.3, for the low and high masses, respectively, that correspond to IMF intervals of 0.1–0.5 and 0.5–100 solar masses. For the stellar evolution model we use the Padova track with thermally pulsating asymptotic-giant-branch (AGB) stars. Three metallicities are considered in the present work, namely $Z = 0.050$, $Z = Z_\odot = 0.020$ and $Z = 0.004$. Finally, our models cover a stellar age range of $10^6$–$10^8$ years with a time resolution of 0.1 Myr.

Based on these assumptions we generate a grid of stellar spectral energy distributions. This stellar atmosphere grid in stellar age and metallicities can be compiled to use as the input radiation source in CLOUDY to study the physical properties of the star formation regions in the galaxy. In order to model an H II region we assume abundances to be the mean of those in the Orion Nebula as determined by Baldwin et al. (1991), Rubin et al. (1991), Osterbrock et al. (1992) and Rubin et al. (1993). Similar to NLR modeling we assume a single-zone, constant density model with hydrogen column densities of $10^{21}$ cm$^{-2}$. In addition, the H II region is characterized by a mixture of graphite and silicate grains typical of those along the Orion Nebula line of sight (Baldwin et al. 1991).

### 3 MID-INFRARED DIAGNOSTICS

Emission-line ratios can be used as a powerful tool to classify emission-line galaxies because they can provide insightful information about the source of ionizing radiation. As a starting point we focus our analysis on mid-infrared diagnostics, in particular the emission-line diagnostic presented in W10 that utilizes three of the most common features observed in the mid-infrared spectra of emission-line galaxies, namely [Ne II], [Ne III] and [O IV] lines. As previously mentioned, the emission-line diagnostic diagram presented in W10 shows a clear separation between the different sources, with the majority of BAT AGN having [O IV]/[Ne III] and [Ne III]/[Ne II] ratios greater than unity; that is, AGN dominated.

#### 3.1 The Active Galactic Nuclei

##### 3.1.1 Single-Zone Model

Figure 1 shows a grid of single-zone photoionization models overlaid on the W10 diagnostic for the BAT AGN sample. For the model grid presented in this comparison we use a range of densities and ionization parameters that are typical of the NLR (Meléndez et al. 2008a, b, 2011). It is clear from Figure 1 that a single-zone approximation misses the majority of BAT AGN by over-predicting the [Ne III]/[Ne II] ratios. This is in agreement with the fact that the [Ne II] emission, given its low ionization potential, may be originating in a different region than that producing the observed higher ionization [O IV] and [Ne III] emission (e.g., Meléndez et al. 2008a).

In Figure 2 we compare the predicted ionic column density and ionization parameter for Ne$^+$, Ne$^{++}$ and O$^{++}$ to find the range of ionization parameters that can maximize these mid-infrared emission lines. This comparison shows that [Ne II] emission peaks at a lower ionization parameter than [O IV] and [Ne III]. However, for log $U < -2.5$, Ne$^+$ and Ne$^{++}$ can coexist in regions with densities of log $n_H \approx 10^3$ cm$^{-3}$ where O$^{++}$ drops sharply. Therefore, in order to simultaneously fit the [Ne III]/[Ne II] and [O IV]/[Ne III] ratios of the BAT AGN, we assume the physical conditions required to maximize [Ne II] emission without increasing the predicted [Ne III]; in other words, a region where only [Ne II] is emitted efficiently. Figure 2 also shows that for densities log $n_H > 10^4$ cm$^{-3}$ there is a drastic change in the relative fraction between Ne$^+$ and Ne$^{++}$. In order to characterize the physical conditions in this region we fit the observed [Ne III]/[Ne II] and [O IV]/[Ne III] ratios for the BAT AGN with a two-zone model.

##### 3.1.2 Two-Zone model

In the two-zone approximation we expect to have a combination of matter- and radiation-bounded materials (e.g., Binette et al. 1996; Meléndez et al. 2011). The matter-bounded component, where the material is optically thin to the ionizing radiation, corresponds to the [O IV] and [Ne III] emitting region, whereas the radiation-bounded component is associated to the [Ne II] efficient region where the material is optically thick. In order to constrain the density in the matter-bounded component we also reproduce the observed [Ne V] 14.32$\mu$m/24.32$\mu$m ratio (see Weaver et al. 2010 for values). In Meléndez et al. (2011) it is found that the densities derived from the [Ne V] ratio are similar to those of the [O IV] emitting region, i.e. a fair assumption for our matter-bounded component.

Figure 3 shows the parameter space that can reproduce simultaneously the observed [Ne III]/[Ne II], [O IV]/[Ne III] and [Ne V] ratios in our two-zone model approximation for the BAT sources. It is clear from this comparison that
there are two distinctive regions, a low-ionization and high-density region where [Ne II] is efficiently emitted (dominated by radiation-bounded models) and a lower density but higher ionization state that corresponds to the [O IV] and [Ne III] region (dominated by matter-bounded models). These parameters are in good agreement with those presented in Meléndez et al. (2008b) for an heterogeneous sample of Seyfert galaxies. According to this parameter-space distribution, the median values for the [Ne II] dominated region are around \( \log U = -4.0 \) and \( \log n_H = 10^{5.5} \text{ cm}^{-3} \), which are in excellent agreement with the maximization of Ne II as implied from its ionic column density (see Figure 2).

In Figure 4 we present our two-zone model grid for the AGN. From the above discussion, we select the median values for the [Ne II] dominated region, namely \( \log U = -4.0 \) and \( \log n_H = 10^{5.5} \text{ cm}^{-3} \), to be those of the radiation-bounded component. Then we select a range of density and ionization parameters for the [O IV] and [Ne III] component. The range of physical conditions for the latter (matter-bounded) are those derived from the individual fit of the mid-infrared ratios of the BAT sources (see Figure 3). Overall, our two-zone photoionization model is in much better agreement with observations; however, it is clear that several BAT AGN still lie outside our two-zone model. These sources, with [Ne III]/[Ne II] and [O IV]/[Ne III] ratios less than unity, have been described as galaxies dominated by star formation (e.g., Meléndez et al. 2008b; Weaver et al. 2010). It must be noted that previous calculations only considered AGN ionization. Therefore these models will always under-predict the observed mid-infrared ratios in the presence of an additional ionizing radiation field from star-formation regions, especially the [Ne II] and [Ne III] luminosities that are good tracers of stellar activity (e.g., Ho & Keto 2007). Additionally, Figure 4 shows that our two-zone model has a lower limit for the [Ne III]/[Ne II] ratio around unity in agreement with observations of AGN dominated sources (e.g., Meléndez et al. 2008b; Weaver et al. 2010).

We have generated a two-zone model grid that can suc-
Figure 4. Comparison between different photoionization models and various observations over-plotted in the W10 diagnostic. We compare observations with three different photoionization models: 1) the two-zone AGN photoionization grid (solid and dashed black lines). On the grid, the solid lines represent density steps with \( \Delta \log n_H = 0.1 \) and the dashed lines ionization-parameter steps with \( \Delta \log U = 0.1 \), see text for details; 2) the single-zone starburst model for a metallicity of \( Z = Z_{\odot} = 0.02 \) and a fixed hydrogen density of \( n_H = 10^{2.5} \text{ cm}^{-3} \). In this model, the solid lines represent a continuous star-formation law and the dashed lines an instantaneous star-formation burst and; 3) the maximum prediction for the [Ne III]/[Ne II] and [O IV]/[Ne III] ratios based on a two-zone starburst model with solar metallicity (gray area). In this model, Equation 2 (dot-dashed line) represents the boundary of our two-zone SB models with solar metallicity. We compare these models with sources from different samples: the BAT AGN sample (red dots), the 12\( \mu \text{m} \) AGN sample (black triangles), the sample of BCD from H09 (green squares) and, H II galaxies from Pereira-Santaella et al. (2010) (blue stars). The dotted line represents the limit between AGN dominated, [Ne III]/[Ne II] > 1, and the star-formation dominated sources.

cessfully reproduce the AGN branch in W10. This analysis is to be extended to other mid-infrared diagnostics, in particular that presented in H09 involving the [Ne III]/[Ne II] and [O IV]/[S III]33.4\( \mu \text{m} \) ratios. The ionization energy to produce [S III] (\( E_{1\mu} = 23.33 \text{ eV} \)) is similar to that for [Ne II] emission, but the high density of the radiation-bounded component will suppress [S III] via collisional de-excitation. On the other hand, given the critical density of the [S III]33.4\( \mu \text{m} \) transition (1.2 \( \times 10^3 \text{ cm}^{-3} \)), this line can be produced in the range of conditions of our matter-bounded component (i.e. the [Ne III] and [O IV] component), albeit with somewhat lower ionization. Therefore, our two-zone model grid should be a good approximation to match the observed AGN branch in this diagnostic, specially at the lower end of the ionization range in the matter-bounded component. Figure 6 also shows good agreement with observations, where it may be seen that our two-zone AGN models are located on the AGN branch different from pure starburst galaxies, probing the effectiveness of this diagnostic in separating emission line galaxies. For this comparison we only use values of Seyfert galaxies from the 12\( \mu \text{m} \) sample Tommasin et al. (2010) where galaxies with detections in all four lines are selected. Note that there are no published values of [S III] for the BAT sample. However, both samples have similar mid-infrared properties (Weaver et al. 2010).

As discussed above, Figure 6 also shows that galaxies with a higher star formation contribution have lower [Ne III]/[Ne II] and [O IV]/[S III]33.4\( \mu \text{m} \) ratios, and fall outside of our two-zone AGN grid.

In general, in order to fit AGN-dominated sources in the W10 diagram (\([\text{Ne III}]/[\text{Ne II}] \) and \([\text{O IV}]/[\text{Ne III}] \) ratios greater than unity), we require an AGN [Ne II] component. This high-density and low-ionization component is justified because of the existence of a number of sources with [Ne II]
emission that show no other signatures of star formation in their mid-infrared spectra; e.g. no detectable PAH features (e.g., Deo et al. 2007; Tommasin et al. 2010; LaMassa et al. 2012; Sales et al. 2014) suggesting that there must be some [Ne II] emission directly associated to the AGN. As seen in Figure 4, this component, where [Ne II] is emitted efficiently, cannot explain the observed emission in many objects where star formation is the dominant ionizing source. As we will discuss below, ionization from stars is more efficient in producing [Ne II] than the harder AGN radiation field (e.g., Meléndez et al. 2008b; LaMassa et al. 2012). Therefore, our [Ne II] AGN component is chosen to represent the maximum (possible) AGN-related [Ne II] emission, but when compared to the total observed flux, this component may be a minimum to the observed [Ne II] emission. It is important to emphasize that, despite the fact that we fix the parameters of the radiation-bounded component to the median of those that can reproduce simultaneously the observed [Ne III]/[Ne II], [O IV]/[Ne III] and [Ne V] ratios, the ionic column density of Ne II is basically insensitive (constant) to changes around these values (see Figure 2), suggesting that our two-zone grid is stable to small differences in the conditions that we selected for the [Ne II] AGN component.

3.2 Starburst Galaxies

3.2.1 Single-Zone Model

Figures 7–9 show a comparison of our models for each mid-infrared ratio presented in the W10 diagram as a function of stellar age, metallicity and star-formation law for a set of conditions typical of H II regions: \(-3.0 < \log U < -1.5\) and \(n_H \sim 10^{2.5} \text{ cm}^{-3}\) (e.g., Rigby & Rieke 2004) with a fixed hydrogen density of \(n_H = 10^{2.5} \text{ cm}^{-3}\) and a set of four ionization parameters.
For both star-formation laws there are dramatic changes in the contribution of stellar populations to the mid-infrared emission lines. Ratios with emission lines that require energies $E > 40$ eV, e.g., [Ne III] and [O IV], have their strongest emission at $\sim 4$ Myr during the Wolf-Rayet phase when WR stars contribute the most to the far-UV flux. After a short time period the burst population becomes very weak at $\gg 6.5$ Myr. For the continuous star formation case after $\sim 6.5$ Myr the stellar population reaches an equilibrium between birth and death (of massive stars) thus becoming time independent. On the other hand, lower-ionization lines such as [Ne II] can be related to the presence of massive main-sequence O stars where they have their biggest contribution at $< 3$ Myr. However, [Ne II] remains strong even at 10 Myr. Interestingly, [Ne II] emission fades away during a short time period, around $\sim 4$ Myr during the WR phase, because the harder photoionizing continuum from WR stars ionizes Ne$^+$ into Ne$^{2+}$. It must be pointed out that the WR phase is very metallicity dependent. Figure 11 shows a comparison for the instantaneous and continuous star-formation case for the number of WR stars and the WR/O ratio from the models as a function of stellar age. As it can be seen from these comparisons, the number of WR stars and the WR/O ratio is highly sensitive to metallicity with a higher prediction of WR stars and longer WR phase in starburst with higher metallicities (e.g., Leitherer et al. 1999).

In Figures 10 and 11 it is important to note that the [O IV]/[Ne III] ratio can only be effectively reproduced after massive O stars have evolved into their WR phase; in other words, according to our synthesis models WR stars are the only source of ionizing photons capable of producing the [O IV] and [Ne V] emission observed in non-AGN sources. Figures 10 and 11 show a comparison between our single-zone starburst photoionization models and a sample of extreme starbursts, blue compact dwarf galaxies presented in H09 over-plotted in the W10 diagram. This model grid covers the range of ionization parameters $-3.0 \leq \log U \leq -1.5$ and a fix density of $n_H = 10^{2.5}$ cm$^{-3}$ and different ionization parameters. Left panels: continuous star-formation law. Right panel: instantaneous star-formation burst.

Figure 6. Comparison between our two-zone AGN photoionization models and the [O IV]/[S III] vs. [Ne III]/[Ne II] diagnostic presented in H09. The dot-dashed line represents the empirical separation between the AGN and the pure star-formation galaxy branch as defined by Equation 1 in H09. On the grid, the solid lines represent density steps with $\Delta \log n_H = 0.1$ and the dashed lines ionization-parameter steps with $\Delta \log U = 0.1$. The red dots represent the Seyfert galaxies from the 12 $\mu$m sample (Tommasin et al. 2010) where we selected galaxies with detections in all four lines.
are not using our grid of photoionization models to predict the emission of individual galaxies but rather to investigate the best range in parameter space for each region in the W10 diagram.

3.2.2 Two-Zone Model

Our single-zone models for an H II region can successfully reproduce the observed [O IV]/[Ne III] < 1 and [Ne III]/[Ne II] > 1 ratios by invoking typical density values and ionization parameters found in H II regions. These ratios in W10 correspond to extreme starburst galaxies such as the one presented in H09 that comprise BCD galaxies, many of which show the optical signatures of WR galaxies. However, our single-zone model fails to predict galaxies with [Ne III]/[Ne II] < 1 and [O IV]/[Ne III] < 1, a region that is characteristic of starburst and H II galaxies. As previously discussed and according to our models, only WR stars have an ionizing continuum capable of producing O IV; therefore, in order to fit the observations of starburst and H II galaxies in this region, a different scenario must be considered.

A possible scenario is the inclusion of an extra ionizing component. In order to reproduce the observed ratios for the H II and starburst galaxies in the W10 diagram, our two-zone model needs to simultaneously maximize [Ne II] and [O IV] emissions. It is worth noting that our two-zone model for star-forming galaxies has many free parameters, e.g., star formation law, metallicity, stellar age, ionization parameter and hydrogen density for each component. Therefore, caution must be taken as the following analysis is based on a set of assumptions that will maximize the amount of [Ne II] and [O IV] emission so as to fit observations for galaxies with [Ne III]/[Ne II] < 1 and [O IV]/[Ne III] < 1 where our single-zone model is inadequate.

Figure 4 shows a comparison between H II galaxies (Pereira-Santaella et al. 2011) and the predicted region for the [Ne III]/[Ne II] and [O IV]/[Ne III] ratios based on our two-zone starburst model with solar metallicity. For the two-zone model we use any combination of an instantaneous star-formation burst within a range of ionization parameters of $-3.0 < \log U < -1.5$ for each zone. The gray region in this comparison represents the location of all the predicted ratios with values [Ne III]/[Ne II] < 1 and [O IV]/[Ne III] < 1 from our two-zone starburst approximation. These are the ratios of the location for the SB/H II galaxies in the W10 diagram. Note that each component in our two-zone model also has a range of stellar age ($10^6 - 10^7$ years) and hydrogen density. From the previous considerations, we perform the quadratic fit

$$\log [\text{Ne III}] / [\text{Ne II}] = -0.27 + 2.79 \times (\log [\text{O IV}] / [\text{Ne III}]) + 1.06 \times (\log [\text{O IV}] / [\text{Ne III}])^2$$

(2)

to the boundary of the maximum contribution from our two-zone model to the W10 diagram.

Equation 2 represents the maximum contribution possible to the W10 diagram derived from our two-zone starburst models with solar metallicity. In other words, it represents the boundary of our two-zone starburst models. Interestingly, Figure 4 shows a few observed sources with ratios outside the previous equation, i.e., outside the starburst region. These sources are NGC 253, NGC 3949, NGC 4157, NGC 520, NGC 5907 and NGC 660. As previously discussed, emission from highly ionized species such as O IV and Ne IV cannot be easily produced by stars because they require a hard photoionizing continuum that can only be produced at a specific period during the WR phase of massive main-sequence stars. Moreover, the duration of the WR phase in these massive stars is highly sensitive to the metallicity of the evolutionary models. Therefore, for galaxies outside our W10 demarcation line one must consider other possibilities such as a weak AGN instead of a population of WR stars (e.g., Lutz et al. 1998) or excitation to high-ionization lines by shocks (e.g., Groves et al. 2004a). Interestingly, some of these sources show evidence for a low-luminosity AGN,
A similar analysis can be carried out with a combination of an instantaneous star-formation burst with subsolar metallicity. Figure 3 shows the predicted region for the [Ne III]/[Ne II] and [O IV]/[Ne III] ratios based on our two-zone starburst model with subsolar metallicity \((Z = 0.004)\). Again, we perform a quadratic fit to the boundaries of our two-zone model:
\[
\log [\text{Ne III}]/[\text{Ne II}] = -0.95 + 1.98 \times (\log [\text{O IV}]/[\text{Ne III}]) + 0.93 \times (\log [\text{O IV}]/[\text{Ne III}])^2 .
\]

Equation 3 represents the boundary of our two-zone starburst models with subsolar metallicity.

It is important to mention that any model combination with a continuous star formation law is unable to reach mid-infrared ratios \([\text{O IV}]/[\text{Ne III}] \gtrsim 0.1\) as seen in Figures 3\(\text{a}\)\(\text{c}\) thus a combination of continuous star formation law models will provide a poor representation to the observed values of starburst and H II galaxies in the W10 diagram. On the other hand, Figures 3\(\text{a}\)\(\text{b}\) show that a combination of AGN and SB models can also reproduce most of the observed line ratios.

\section{OPTICAL DIAGNOSTICS}

In Section 3\(\text{b}\) we have discussed various photoionization models that can successfully reproduce emission-line galaxies in different mid-infrared diagnostics, ranging from pure starburst to AGN. In this respect, we use our mid-infrared models to predict some of the most commonly used emission-line ratios in optical classification diagrams, e.g. \([\text{O III}]/\beta\) and \([\text{N II}]/\text{H} \alpha\), to establish new classification parameters. For the present work we have compared our theoretical predictions with a sample of galaxies from SDSS DR8. The galaxy spectra for DR8 refer to the measurements and techniques developed at the Max Planck Institute for Astrophysics and the Johns Hopkins University (the MPA-JHU measurements are based on the methods of Birmann et al. 2004; Tremonti et al. 2004). Our SDSS sample was selected to have a S/N>~3σ for the four emission lines in the [O III]/\beta\) and [N II]/\text{H} \alpha\) ratios resulting in a total of 411,010 galaxies.

\subsection{New Classification Parameters}

The origin of \(\text{N}^+\) emission, giving its low ionization potential \(E_{\text{IP}} = 14.53 \text{ eV}\), can be associated to the same source of ionizing radiation as \(\text{Ne}^+\) emission; however, the [N II]6583 (hereafter [N II]) line has a critical density \((6.6 \times 10^3 \text{ cm}^{-3})\) roughly one order of magnitude lower than [Ne II] \((7.1 \times 10^3 \text{ cm}^{-3})\). Therefore, in our two-zone AGN approximation, the high-density radiation-bounded component where the [Ne II] is emitted efficiently represents a conservative lower limit for [N II] emission. Figure 11 shows the radius-averaged ionization fraction for \(\text{N}^0\), \(\text{N}^+\) and \(\text{N}^{++}\) for a range of densities and ionization parameters, where it can be seen that, for the set of conditions that maximize [Ne II] emission (Figure 3), most of the nitrogen is neutral and only a small fraction (\(\sim 20\%\)) is singly ionized. Additionally, the high density in the radiation-bounded component is suppressing [N II] emission via collisional de-excitation. Therefore, it is clear that the physical conditions in the [Ne II] emitting region are not optimal for producing [N II]; however, even under these unfavorable conditions, a small fraction of \(\text{N}^+\) can exist. As a result, our two-zone grid is not intended to fit the entire AGN branch in the optical [O III]/\beta\) and [N II]/\text{H} \alpha\) diagram, but to provide a reliable lower-limit to the AGN contribution in these optical emission lines. Moreover, the stability of this lower-limit relies on the fact that the predictions from the [Ne II] AGN component are nearly independent to small changes around the values that we set for the radiation-bounded component.

Figure 12 shows the optical predictions from our two-zone AGN approximation (see Figure 3\(\text{b}\) overlaid on our SDSS sample for the [O III]/\beta\) vs. [N II]/\text{H} \alpha\) diagram. It may be appreciated that our two-zone grid under-predicts the observed [N II]/\text{H} \alpha\) as previously discussed. On the other hand, [O III] emission can originate in a region with very similar conditions to [Ne III] and [O IV] emission (e.g., Meléndez et al. 2008). The physical conditions of the [Ne III] and [O IV] emitting region are in good agreement with those inferred by Baskin & Lau (2003) from the simultaneous fit of the equivalent width of the narrow [O III], [O III]λ4363 and \(\text{H} \beta\) lines in the Palomar-Green quasar sample; in particular to those conditions in the outer region in their two-zone approximation, where most of the [O III] is emitted. Therefore, our matter-bounded component can efficiently produce the observed [O III]/\beta\). We can then identify a lower-bounded demarcation line for our models corresponding to a constant ionization parameter of \(\log U = -1.5\). This value for the ionization parameter is where the radius-averaged ionization fraction of \(\text{O}^{++}\) decreases as this species gets ionized into \(\text{O}^{+3}\) (see Figure 13). In other words, this lower-bounded demarcation line represents an ionization parameter where the \(\text{O}^{+3}\) surpasses the ionization fraction of \(\text{O}^{++}\); therefore, the gas is inefficient in producing [O III] emission, thus, a reasonable limit for our models. In addition, \(\log U = -1.5\) is the limit found by Baskin & Lau (2003) in the distribution of ionization parameters for the outer region in their two-zone approximation. From a nonlinear fit of the two-zone photoionization
model with a fixed \( \log U = -1.5 \), we define a galaxy to have an AGN component if

\[
\log \left[ \frac{[O \text{ III}]}{H\beta} \right] > \frac{0.12}{\log \left( \frac{[N \text{ II}]}{H\alpha} + 0.34 \right)} + 1.15 .
\]

This demarcation line is the lowest theoretical prediction for the AGN contribution to the optical spectra, and lies above the star-formation branch of the \( \log \left[ \frac{[O \text{ III}]}{H\beta} \right] vs. \log \frac{[N \text{ II}]}{H\alpha} \) diagram predicting a lower number of pure star-forming galaxies than Ka03. In fact, the Ka03 demarcation line separates our SDSS sample into \( \sim 65\% \) pure star-forming galaxies (266,696 sources) and \( \sim 35\% \) AGN (144,314 sources), while our definition leads to a separation of the sample of \( \sim 51\% \) pure star-forming galaxies (208,977 sources) and \( \sim 49\% \) AGN (202,033 sources). Note that in our AGN dominated models any extra contribution from star-forming regions can only move objects above the AGN lower-bound demarcation line (Ke01) as we push into more favorable conditions for \( [N \text{ II}] \). Therefore, sources above this line may have different stellar contributions to their optical spectra, ranging from composite systems to AGN dominated sources. Figure 13 shows a comparison between our new AGN demarcation line and those from Ke01 and Ka03. Overall, our AGN models predict a higher AGN population by a factor of \( \sim 1.4 \) than predictions derived from a semi-empirical division of star-forming galaxies (K03).

The expression for the boundary between star-forming galaxies and AGN, namely Equation 3 is in agreement with the theoretical curve presented by Stasińska et al. 2006), which is the demarcation between “pure” star-forming galaxies and galaxies hosting an AGN. This line represents the set of stellar models that best reproduce the upper envelope of the left wing in the \( \log \left[ \frac{[O \text{ III}]}{H\beta} \right] vs. \log \frac{[N \text{ II}]}{H\alpha} \) diagram. Using this curve, our SDSS sample is divided into \( \sim 49\% \) pure star-forming galaxies (203,156 sources) and \( \sim 51\% \) AGN (207,854 sources), similar to the cut from our line. Interestingly, our curve lies above that from Stasińska et al. 2006) with a large gap above the left wing (star-formation branch) in the optical diagram. It is important to point out that the predicted ionization fraction for highly ionized ions is density independent in the optically thin, matter-bounded component. On the other hand, the ionization fraction in our optically thick, radiation-bounded models with more lowly ionized ions is very density sensitive (see Figures 11 and 13).
We can define a theoretical limit for the maximum AGN contribution to the optical diagram based on a two-zone approximation. For this purpose, we simultaneously fit the observed [O III]/Hβ and [N II]/Hα ratios for each AGN in our SDSS DR8 sample with a two-zone model grid spanning ranges of the ionization-parameter \((-3.5 \leq \log U \leq -1.5\) and hydrogen density \((2.0 \leq \log n_H \leq 5.5 \text{ cm}^{-3}\)) for each component. These parameter ranges are typical of the AGN NLR, including the conditions driving [O III] emission (e.g., Baskin & Laor 2005; Meléndez et al. 2008; Pereira-Santaella et al. 2010), and moreover, are consistent with the set of conditions derived from the ionization fraction for these lines (see Figure 11 and Figure 13). Figure 14 also shows the result of a nonlinear fit to the upper-bound region derived from our models from which we define the maximum AGN line

\[
\log \frac{[\text{O III}]}{H\beta} = \frac{0.16}{(\log \frac{[\text{N II}]}{H\alpha} - 0.17)} + 1.31
\] (5)

This line represents the maximum AGN contribution to the optical spectra given by the set of conditions adopted in our AGN models, but it is clear that a number of AGN lie above it. To reach this extreme upper-right region in the AGN branch our models need to increase the predicted [O III]/Hβ and [N II]/Hα ratios. A possible way is to increase the oxygen and nitrogen abundances taking into account that at high-metallicity they scale proportionally (e.g., Groves et al. 2004a). An alternative way would be to increase the hydrogen column density in the models resulting in a combination of radiation-bounded regions that will increase [O III] and [N II] production (e.g., Meléndez et al. 2011). Given the number of free parameters, we are unable to provide a unique scenario to explain the AGN-branch high end in the [O III]/Hβ and [N II]/Hα diagram above our AGN maximum demarcation line and outside our parameter space.

As previously mentioned, our AGN photoionization models are dust free; however, to study the effect of dust on our demarcation lines, we generate a new set of models where grains mix with the emission-line gas. We include graphite and silicate grains with a size distribution and a dust-to-gas ratio half of the value for the Galactic interstellar medium (ISM) (Mathis et al. 1977). This dust-to-gas ratio is based on the high angular resolution analysis of the Hubble Space Telescope (HST)/Space Telescope Imaging Spectrograph (STIS) of the NGC 4151 and NGC 1068 Seyfert galaxies (Kraemer et al. 2004; Kraemer & Crenshaw 2000). From these models we have derived

\[
\log \frac{[\text{O III}]}{H\beta} > \frac{0.13}{(\log \frac{[\text{N II}]}{H\alpha} + 0.31)} + 1.24
\] (6)

Equation 6 represents the AGN demarcation line including dust and the same set of physical conditions derived from our dust-free models (Equation 4). Figure 15 gives a demarcation line comparison with and without dust, where it may be seen that dust has a small effect on our theoretical line in the [O III]/Hβ vs. [N II]/Hα diagnostic diagram.

Similarly, in Figure 16 we overlay our single-zone starburst optical predictions with solar metallicities on our SDSS sample in the [O III]/Hβ vs. [N II]/Hα diagram. From this comparison it is found that our single-zone models for starburst galaxies are a good match to the pure star-formation branch of galaxies with the ionization parameter decreasing with metallicity toward low [N II]/Hα and high [O III]/Hβ. Our results are in excellent agreement with previous estimates based on the theoretical modeling of the maximum starburst contribution line presented in Ke01 and the empirical demarcation line presented in Ka03 between pure SB/H II galaxies and sources with some AGN contribution to their optical spectra. As previously discussed, our two-zone starburst models are extremely sensitive to a number of parameters that can lead to some degeneracy; for this reason and for the sake of simplicity, we do not show a comparison between our two-zone predictions and the SDSS sample.

5 CONCLUSIONS

We have carried out extensive and detailed photoionization modeling to successfully locate different emission lines galaxies in optical and mid-infrared diagnostic diagrams. Our model grids cover a wide range in parameter space for the non-thermal AGN continuum and starburst galaxies with different stellar population laws and metallicities. As a result we arrive at the following findings.

(i) We successfully reproduce the AGN region in the W10 diagram with a two-zone model: [O IV]/[Ne III] > 1 and [Ne III]/[Ne II] > 1. This model is a combination of radiation-bounded (high density and low ionization) and matter-bounded (low density and high ionization) components that efficiently produce [Ne II] and [Ne III]−[O IV] emissions, respectively.

(ii) Overall, our single-zone starburst models are a good fit to the extreme starburst region in the W10 diagram, i.e. [O IV]/[Ne III] < 1 and [Ne III]/[Ne II] > 1, for which the
Figure 16. Comparison between the SDSS sample and the predicted optical emission lines derived from our single-zone mid-infrared SB models. The SB models presented here are the same as in Figure 4. The dashed and solid lines represent the same stellar law as in Figure 4. The dotted line is the empirical demarcation presented in [Kauffmann et al. (2003)] (Ka03). The solid line is the theoretical demarcation line for the maximum contribution calculated in [Kewley et al. (2001)] (Ke01).

An instantaneous star-formation burst provides the best fit. In addition, our subsolar models are able to reach the highest \([\text{O IV}]/[\text{Ne III}]\) values in agreement with the location of low-metallicity starburst galaxies.

(iii) The two-zone starburst approximation for an instantaneous star-formation burst provides the best fit to the star-forming region in the W10 diagram, i.e. \([\text{O IV}]/[\text{Ne III}] < 1\) and \([\text{Ne III}]/[\text{Ne II}] < 1\). However, we find that any combination of purely continuous star formation cannot reproduce the \([\text{O IV}]/[\text{Ne III}]\) ratios observed in most of the star-forming galaxies. We define new regions and demarcation lines in the W10 diagram based on the maximum star-formation contribution derived from these models.

(iv) We investigate the optical predictions from our two-zone AGN mid-infrared photoionization grid using the \([\text{O III}]/\beta\) and \([\text{N II}]/\text{H}\alpha\) diagnostic diagram. Given the high density and low ionization of the radiation-bounded component in our two-zone AGN model, we find this region to be a good lower limit to \([\text{N II}]\) emission in agreement with the ionization fraction and the critical density of \(N_\text{II}\). In other words, the physical conditions in the \([\text{Ne II}]\) emitting region are not optimal for producing \(N_\text{II}\); however, even under these conditions a small fraction of \(N_\text{II}\) can exist. Therefore we define a new theoretical demarcation line for the minimum AGN contribution to this optical diagnostic diagram. As a result we find that our new classification estimates a higher AGN population by a factor of \(\sim 1.4\) than predictions derived from a semi-empirical division of star-forming galaxies (K03). Moreover, our classification is in good agreement with the semi-empirical starburst demarcation line from [Stasińska et al. (2006)].

(v) We define a maximum AGN contribution in the \([\text{O III}]/\beta\) and \([\text{N II}]/\text{H}\alpha\) diagram based on a two-zone approximation represented by the combination of any two regions within a range of parameters to maximize the emission of these optical lines. The range of physical parameters relies on our predictions of the ionization fractions and ionic column densities of these ions and is in agreement with typical NLR parameters.

Overall, we use a grid of AGN models to define a new set of demarcation lines that are useful in classifying galaxies. Our theoretical models provide a new perspective into the non-thermal ionizing AGN continuum, and are intended to complement previous studies that rely solely on the contribution from the stellar ionizing radiation field.

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