Finite Element Stress Analysis of Acrylic with Embedded Optical Fibre Sensors

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Abstract. Finite element (FE) techniques are used to analyse mechanical stress in optical fibre sensors embedded in acrylic. The models represent many features observed in real materials with embedded fibre optic for stress and strain sensor application such as for health monitoring of structures. Three thicknesses, namely 6 mm, 8 mm and 10 mm of acrylic were analyzed with the optical fibre embedded at the mid-plane of acrylic. The simulation was done by implementing Finite Element Method using ABAQUS software. Contact between acrylic and optical fibre was modelled as frictionless and with friction. The friction coefficient was varied for various values which are 0.3, and 0.5. This paper investigates the effect of friction coefficient and the effect of fibre optic’s depth embedded in acrylic to the their von Misses stress. Simulation result shows that the higher the friction coefficient the higher von Misses stress in fibre optic and the higher von Misses stress in acrylic. The higher the fibre’s depth the higher von Misses stress in fibre and the lower von Misses stress in acrylic. The maximum stress occurred for the coefficient of friction 0.5, with magnitude of 116.4 MPa and 58.72 MPa for acrylic and optical fibre respectively. The most significant effect of fibre’s depth to the von Misses stress was obtained for 1 mm depth for acrylic and 5 mm for optical fibre, with magnitude of 72.64 MPa and 57.65 MPa for acrylic and optical fibre respectively.

1. Introduction

Fibre optic as sensor has many advantages namely: small size, light weight and immunity to electromagnetic interference [1]. Fibre optic sensor with these advantages can be embedded into the host material to form an ideally smart structure system. Nowadays fibre optic has been used as sensor in many applications such as for structural health monitoring and aerospace engineering, industrial processing and defence industry [2-8]. The information on numerous important parameters such as micro strain, micro vibration, and stiffness, which are vital to the in situ structural health monitoring as well as the optimizations of the system performances can be obtain from embedded fibre optic sensor [9-18].

Fibre optic has been embedded in some material as a pressure sensor in health monitoring of structures and bridges. Acrylic has been used widely for roof and wall of some buildings. Therefore, to ensure the safety of fibre optic that embedded in acrylic it is necessary to investigate the stress condition inside the fibre optic under pressure load. Some researchers have carried out the stress analysis embedded in composites and other materials [3], [11-12], [14-16], [19-24]. The contact condition between fibre optic and acrylic has also been defined and varied as frictionless and with certain various
friction coefficient, namely 0.3, 0.5 and 0.8. The depth of fibre optic embedded in acrylic also will be varied by 1mm until 5 mm. The effect of friction coefficient and the depth of fibre optic was embedded in acrylic will be investigated in this research using FE simulation technique.

2. Finite Element Simulation

2.1. Acrylic and fibre optic model
Model of fibre optic embedded in acrylic has been drawn using Solid works software. The model depicted in Figure 1, for acrylic and fibre optic respectively. The fibre optic was modelled as a solid rod with diameter of 1 mm, and the acrylic has a 50 mm in length and 40 mm in width, with various of thicknesses, 6 mm, 8 mm and 10 mm. The material properties of acrylic and fibre optic were shown in Table 1.

![Figure 1. Model (a) Acrylic; (b) fibre optic](image)

| Mechanical Property                  | Material  |
|--------------------------------------|-----------|
|                                      | Fibre Optic | Acrylic |
| Density (kg/m³)                      | 7200      | 7850    |
| Ultimate Tensile Strength (MPa)      | 450       | 450     |
| Tensile Yield Strength (MPa)         | 280       | 435     |
| Modulus of Elasticity (MPa)          | 140       | 190     |
| Poisson's Ratio                      | 0.211     | 0.27    |
2.2. Load and boundary condition

Load was given as distributed pressure on top of surface of acrylic with fibre optic has embedded inside. The magnitude of pressure is 80 MPa. That magnitude was considered according to maximum pressure that can be applied to the acrylic with has 6 mm in thickness.

There are two boundary conditions (BCs) on the model. First boundary condition is fixed that was applied in the bottom of the acrylic, this BC restricted the model to translate and rotate in all directions. The second BC was applied on both of two ends of fibre. This kind of BC restricted the fibre translation in axial direction and restricted rotation in all directions. Figure 2 show the load and two boundary conditions of the model.

![Figure 2](image)

(a) (b) (c)

**Figure 2.** Load and Boundary Condition; (a) Load; (b) BC 1; (c) BC 2

3. Result and Discussion

The simulation result of von Misses stress for fibre with various coefficients of friction were shown in Figure 3 for 4 mm thickness of acrylic and 1 mm of fibre’s depth. The maximum von Misses stress of acrylic for frictionless contact condition is 64.04 MPa, while the von Misses stress for coefficient of
friction 0.3 is 116.4 MPa. The von Misses stress of acrylic tend to increase by increasing the coefficient of friction.

Figure 3. Von Misses stress in acrylic of 4 mm acrylic thickness; (a). for frictionless condition; (b). for 0.3 coefficient of friction

Von Misses stress simulation result for 4 mm thickness of acrylic and 1 mm of fibre’s depth can be seen in Figure 4. The trend of stress in the fibre also same with that of stress in the acrylic. The stress is increase by increasing of coefficient of friction.
Figure 4. Von Misses stress in fibre of 4 mm acrylic thickness; (a). for frictionless condition; (b). for 0.3 coefficient of friction.

The relation between von Misses stress and the coefficient of friction was stated in Figure 5. The von Misses stress of both acrylic and fibre were increase by increasing of coefficient of friction.

Figure 5. Effect of the coefficient of friction to the stress in fibre optic and acrylic for 1 mm depth.

Figure 6 shows the von Misses stress of acrylic for 8 mm thickness of acrylic and 3 mm of fibre’s depth, frictionless condition. It can be seen that the maximum von Misses stress was occurred at near of surface with magnitude of 64.67 MPa, while the acrylic with 1 mm of fibre’s depth has the von Misses stress of 72.46 MPa which occurred at the surface of acrylic which contact with fibre.
Figure 6. Von Misses stress in acrylic of 8 mm acrylic thickness (frictionless); (a) for 3 mm of fibre’s depth; (b) for 1 mm of fibre’s depth.

Figure 7 shows the von Misses stress of fibre for 8 mm thickness of acrylic and 3 mm of fibre’s depth, frictionless condition. It can be seen that the maximum von Misses stress was occurred at surface near to the right end of fibre with magnitude of 70.32 MPa, while the fibre with 1 mm of fibre’s depth has the von Misses stress of 57.65 MPa which occurred at the same region with that of 3 mm of fibre’s depth.

Figure 7. Von Misses stress in fibre of 8 mm acrylic thickness (frictionless); (a) for 3 mm of fibre’s depth; (b) for 1 mm of fibre’s depth.

The relation between von Misses stress and the fibre’s depth was displayed in Figure 8. The von Misses stress of fibre was increase by increasing of fibre’s depth, but the von Misses stress of acrylic was decrease by increasing of fibre’s depth.
4. Conclusion
The stress analysis of fibre optic sensor embedded in acrylic was accomplished by finite element method. Based on the simulation result, it can be concluded that von Misses stress of fibre optic and acrylic were increase by increasing of coefficient of friction. The von Misses stress of fibre was increase by increasing of fibre’s depth, but the von Misses stress of acrylic was decrease by increasing of fibre’s depth. The maximum von Misses stress of acrylic and optical fibre sensor was occurred for the coefficient of friction of 0.5, for 1 mm depth the magnitude of stress is 116.4 MPa and 58.72 MPa for acrylic and optical fibre respectively. The maximum von Misses stress for fibre’s depth variation was occurred at 1 mm for acrylic and 5 mm depth for optical fibre, with magnitude of 72.64 MPa and 57.65 MPa for acrylic and optical fibre respectively.

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