Microwave-assisted seed preparation for producing easily phase-transformed anatase to rutile†

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Titanium dioxide (TiO₂) is an inorganic chemical well known for its good optical performance, inertness and environmentally friendly chemical properties, and it is widely used in pigments, papermaking and ceramics. Of the two main kinds of crystal TiO₂, rutile has better pigment properties than anatase. In the commercial sulfate process, rutile-form TiO₂ product is obtained by crystal transformation of anatase in a high-temperature calcination (>1000 °C) in the absence of a crystal transforming agent. And some studies also show that a calcination under 900 °C over 2 h is necessary to ensure full crystal transformation.

Hydrolysis is the most important operation in the sulfate process. A narrow particle size distribution (around 1–2 μm) of the hydrolysis particles is the key factor to obtain good optical properties of the final product. Early hydrolysis operations were conducted by self-generating nuclei crystallization, in which particle size control is very difficult. The initial nucleus seeds are formed by dropping the titanyl sulfate solution into hot water. Because the crystal growth is non-reversible, the initial nuclei decide the final particle size distribution and the particle activities. The self-nucleation process is an unstable process, which is greatly influenced by parameter control.

By adding nucleus seeds, the hydrolysis process can be well controlled. The nucleus seeds are usually called external crystal seeds. Ideal nucleus seeds are in the range of 2–3 nm with a narrow size distribution, and their dosage in hydrolysis is about 1–2.5%. The seeds are generally prepared by neutralizing titanyl sulfate solution with hot sodium hydroxide solution, in which the seed properties are dependent on the reaction conditions, such as temperature, feed ratio and addition rate.

However, the present hydrolysis process cannot afford high-crystal-transfer active metatitanic acid. And the titanyl sulfate solution is required to be concentrated from 120 g L⁻¹ to 180–
220 g L\(^{-1}\) in order to match the needs of hydrolysis. This results in the consumption of much energy in evaporation.

With the development of microwave technology,\textsuperscript{30–34} microwave-assisted technology is successfully used to synthesize nanometer titanium dioxide materials.\textsuperscript{35–40} In this work, a novel hydrolysis method was developed, in which microwave-assisted technology was applied in the preparation of nucleus seeds. The technology can produce uniform and active seeds, and the seeds can induce the hydrolysis of dilute titanyl sulfate solution and result in uniform precipitate particles. The hydrolysis particles are highly active in the following calcination operation and are easily converted to rutile TiO\(_2\) at a lower temperature in the absence of a rutile crystal transforming agent.

2. Experimental

The titanyl sulfate solution used for hydrolysis was prepared by using titanyl sulfate powder (Guangfu Chemical Research Institute, Tianjing, CP) and ferrous sulfate (Kermer, Tianjing, AR) to form a solution with a concentration of 160 g L\(^{-1}\) of TiO\(_2\) and a Fe/TiO\(_2\) mass ratio of 0.3. And the sulfuric acid mass was 1.9 times of titanium dioxide mass.

The titanyl sulfate solution for seed preparation was prepared from the same titanyl sulfate source in absence of ferrous sulfate. The titanyl sulfate solution with a given concentration was heated in a microwave oven (Panasonic NN-GF352M) for several seconds to obtain a seed sol. The solution was called the seed titanyl solution (STS). The stability of the seed sol was measured by the dilution method, in which 10 mL seed sol was diluted by adding water until the sol turned turbid. The stability of the seed sol is defined as the ratio of the volume of added water to the volume of seed sol:

\[
S = \frac{V_1}{V_2}
\]

where \(V_1\) is the volume of water added and \(V_2\) is the volume of seed sol.

Hydrolysis was conducted inside a 100 mL three necked flask with agitation under atmospheric pressure. In each batch, 50 mL of titanyl sulfate solution (the solution was called the hydrolysis titanyl solution (HTS)) was heated to 90–96 °C and then about 2% (mass ratio referring to titanium dioxide mass) seeds were inoculated. Keeping agitated at the temperature for 10 min, the reactants were heated to boiling point (namely the first boiling point) and heating maintained for several minutes until the solution turned gray. After stopping heating and stirring, the slurry was aged for 30 minutes. And then, agitating again and heating to boiling point (namely the second boiling point) again,\textsuperscript{41} the slurry was hydrolyzed for another 3.5 hours. At last, the slurry was filtered and washed with 10% sulfuric acid solution and distilled water. The hydrolysis metatitanic acid, the filtration cake, was calcined at 850 °C in a muffle furnace for 30 minutes, and then cooled to room temperature.

The hydrolysis ratio was calculated as follows:

\[
Y = (1 - \frac{m_1}{m_2}) \times 100\% + 0.5
\]

where \(m_1\): titanium dioxide concentration in slurry; g L\(^{-1}\), \(m_2\): titanium dioxide concentration in the filtrate; g L\(^{-1}\), 0.5: the corresponding number.\textsuperscript{41}

The metatitanic acid particle size distribution was characterized by a particle size analyzer instrument (Runzhi Rise-2002). And the particle size of the seeds was characterized by a Marvin nano-size analyzer instrument.

The XRD characterizations were carried out with a DX-2700 X-ray diffractometer. The voltage and anode current were 40 kV and 30 mA, and Cu K\(_\alpha\) = 1.5406 nm and continuous scanning mode with 0.03 interval and 0.05 s set time were used to collect XRD patterns.

Scanning electron microscopy (SEM) studies were carried out with a JEOL 7610F electron microscope to examine the morphology of hydrolysis products and calcination products.

3. Results and discussion

In commercial hydrolysis operation, nucleus seeds are often used to initiate hydrolysis in the sulfate TiO\(_2\) process. It not only leads to a high hydrolysis ratio, but also ensures a narrow size distribution of products.\textsuperscript{3,27} In this work, the influence of microwave-assisted seed preparation on hydrolysis behaviors is discussed in detail. The products so obtained were analyzed and the following calcination was optimized. The seed properties significantly affect the crystal transformation of the product from anatase to rutile.

Parameter tests, including the microwave heating parameters and hydrolysis parameters, were conducted and the results are discussed in the following.

3.1 Effects of microwave conditions on hydrolysis

3.1.1 The hydrolysis behaviors. Microwave heating rate greatly influences the hydrolysis and crystallization of the titanyl solution. In the preparation process, the heating rate depends on the microwave power, which decides the seed behaviors. The microwave heating power was investigated in the range from 200 W to 800 W, and microwave heating time varied from 30 s to 100 s, respectively. In all seed preparations, referring to the solution component in industrial processes, the Fe/TiO\(_2\) (mass ratio) and H\(_2\)SO\(_4\)/TiO\(_2\) (mass ratio) of the initial titanyl solution were maintained at 0.3 and 1.9, respectively.

The results showed that microwave heating parameters significantly affected the seed stability and the hydrolysis ratio. In the range of 200 to 800 W, the hydrolysis ratio increased with heating power and the stabilities of the seeds decreased (Table 1, no. 1–4). This means that high heating power during 60 s of given time resulted in a high activity of seeds. On the other hand, decreasing heating time also resulted in a hydrolysis ratio decrease and stability increase. However, 70 s of heating time led to a decrease of hydrolysis ratio. When the energy was suitable for seed formation, the seeds were mainly titanic acid. When more energy was involved in the seed preparation process, it would lead to oversaturated seeds, in which metatitanic acid seeds formed. Then the seeds would become grey, and active seed numbers decreased.\textsuperscript{14,16,42} To clarify the
relationship between the STS concentration and the microwave energy injected, experiments (as shown in Table 1, No. 1 and 9–12) were carried out. With an increase of the STS concentration, more microwave heating energy is required to ensure seed stability, but the hydrolysis ratio decreased slightly. The hydrolysis particles were almost the same, as shown in Fig. S1 and Table S1.

To further evaluate the effects of the microwaves on the hydrolysis kinetic behaviors, the hydrolysis time with different microwave heating times of seed preparation were investigated as shown in Fig. 1. The hydrolysis time observed was up to 5 h, while the microwave heating times of seeds preparation were 30 s, 40 s, 50 s and 60 s. The heating power was 800 W, and all the other conditions were the same as shown in Table 1.

As shown in Fig. 1, all the final hydrolysis ratios in 5 hours reached 90%. But the hydrolysis reaction rates are different when using different seeds; they increased with the increasing of heating time in seed preparation. When heating for 60 s in seed preparation, the seed stability was 10 and the following hydrolysis process finished in 3.5 h. And for 50 s and 40 s, the seed stabilities were 15 and >20, and the complete hydrolysis times were 4.5 h and 5 h, respectively.

To understand the kinetic behaviors of the hydrolysis with microwave-assisted seeds, the hydrolysis results (as shown in Fig. 1, before hydrolysis equilibrium) were fitted with kinetic equations,

\[ \ln \frac{C_t}{C_0} = kt \]

from which the hydrolysis process turned out to be a secondary autocatalytic reaction, these results being shown in Fig. 2 and Table 2, where the hydrolysis rate constants decreased with the microwave heating time decreasing.

3.1.2 The hydrolysis particles. The hydrolysis particle size distributions influence the TiO₂ product size distributions and the pigment properties. Sizes were measured by a particle size analyzer instrument. The results were obtained and then fitted with a lognormal distribution. The particle size distribution

Table 1 Hydrolysis ratio under different operating conditions

| No. | STS concentration (g L⁻¹) | Heating power (W) | Heating time (s) | Seed stability | Hydrolysis ratio (%) |
|-----|--------------------------|-------------------|-----------------|---------------|----------------------|
| 1   | 30                       | 800               | 60              | 10            | 95.4                 |
| 2   | 30                       | 600               | 60              | 15            | 91.8                 |
| 3   | 30                       | 400               | 60              | >20           | 89.1                 |
| 4   | 30                       | 200               | 60              | >20           | 71.4                 |
| 5   | 30                       | 800               | 70              | *             | 72.0                 |
| 6   | 30                       | 800               | 50              | 15            | 86.0                 |
| 7   | 30                       | 800               | 40              | >20           | 67.3                 |
| 8   | 30                       | 800               | 30              | >20           | 57.1                 |
| 9   | 33                       | 800               | 70              | 10            | 94.7                 |
| 10  | 40                       | 800               | 80              | 10            | 93.9                 |
| 11  | 45                       | 800               | 90              | 10            | 91.9                 |
| 12  | 50                       | 800               | 100             | 10            | 90.6                 |

* All hydrolysis tests were carried out as follows: HTS concentration was 160 g L⁻¹; Fe/TiO₂ mass ratio was 0.3, H₂SO₄/TiO₂ mass ratio was 1.9. The seed addition was 2%; temperature was 104 °C; hydrolysis time (after the second boil point) was 3.5 h. *The seeds turned grey, meaning precipitation could be observed.

Fig. 1 Hydrolysis ratios for different microwave heating times.

Fig. 2 The hydrolysis kinetic results of microwave seeds under different microwave heating times.
results of the hydrolysis particles under different microwave conditions are shown in Fig. 3 and Table 3.

Microwave heating rate greatly affects the properties of seeds and the following hydrolysis activities. Fig. 3 shows that the hydrolysis particle size distribution widens gradually with decreasing heating power, according to the results in Tables 1 and 3. The hydrolysis ratio increased from 71.4% to 95.4%; however, the mean diameter slightly decreased from 1.935 μm to 1.887 μm and the variance of the particle size distribution decreased from 0.260 to 0.231. And the same phenomenon could be found with the microwave heating time decreasing as shown in Fig. S2.† This means that the hydrolysis particles produced with the seeds of lower microwave intensity are less uniform than the particles of a higher microwave intensity. This suggested that the seed apparent activity would increase with increasing microwave intensity, and this would be the key factor for both hydrolysis rate increasing and a narrow hydrolysis particle size distribution.

Microwaves usually provide an integral temperature field in chemical synthesis. And in this work they were used to heat the seeds rapidly and integrally, which would lead to uniform seeds for hydrolysis (particle size of seeds shown in Table S2†). Since the microwave-assisted methods always prepare uniform products, the activity of each seed could be considered even. Combining with the hydrolysis particle distribution results (as shown in Table 1 and Fig. S2†), it suggests that the number of seeds formed under microwave conditions would decrease with a decrease of the microwave energy injected. The microwave heating effect on the seed preparation was proposed and it was compared with the traditional self-generating nuclei process (as shown in Fig. 4). With a lower number of seeds in the initial hydrolysis solutions, the apparent hydrolysis activity decreased and uncontrolled self-generating nuclei would easily form, which leads to a wider hydrolysis particle distribution. And as a result, the particle size distribution became wider, and the particle size increased slightly.

The final particle size was basically similar at the hydrolysis time observed, indicating that the microwave heating seems not to be the major factor affecting the original seed activity and the particle size (as shown in Table 3 and Fig. 3). But it affects the seed apparent activity formed in the seed preparation. It suggests that the seed number would be quite different with the microwave energy injected. As we discussed above, the microwave energy injected affects the seed stability, which would lead to different hydrolysis rates and different hydrolysis ratio of metatitanic acid. In an appropriate microwave energy range, the greater the microwave energy injected in the seed preparation, the more effective seeds would form. As a consequence, the seeds would be less stable but with a higher apparent activity, which could be represented as the hydrolysis rate. And the hydrolysis ratio would increase with the particle size and particle size distribution of metatitanic acid widens with the hydrolysis time increasing.

### 3.2 Effects of hydrolysis conditions

Hydrolysis conditions were optimized and the results are shown in Table 4. Fe/TiO₂ and H₂SO₄/TiO₂ ratios varied in the range of 0–0.4 and 1.9–2.5, and all these conditions are close to those of commercial processes. The amount of seeds added was changed in the range from 0.5 to 2.5 wt%.

The hydrolysis ratio varied with H₂SO₄/TiO₂ markedly, while the Fe/TiO₂ mass ratio did not much influence the hydrolysis ratio. With the Fe/TiO₂ mass ratio increasing, the hydrolysis increased slightly after a slight decrease. And all the hydrolysis

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**Table 2** The hydrolysis rate constants for different seed microwave heating times

| Seed microwave heating time (s) | Rate constant (L mol⁻¹ h⁻¹) | Correlation coefficient ($R^2$) |
|--------------------------------|-----------------------------|-------------------------------|
| 60                             | 1.256                       | 0.95                          |
| 50                             | 1.143                       | 0.99                          |
| 40                             | 0.947                       | 0.98                          |
| 30                             | 0.872                       | 0.98                          |

† The HTS concentration was 160 g L⁻¹, the STS concentration was 30 g L⁻¹, the microwave heating power was 800 W, the Fe/TiO₂ ratio was 0.3 and the H₂SO₄/TiO₂ ratio was 1.9. The hydrolysis temperature was 104 °C.

**Table 3** The variance for different particle size distributions

| No. | Heating power (W) | Mean diameter (μm) | Variance |
|-----|-------------------|--------------------|----------|
| 1   | 800               | 1.887              | 0.231    |
| 2   | 600               | 1.899              | 0.254    |
| 3   | 400               | 1.921              | 0.248    |
| 4   | 200               | 1.935              | 0.260    |

† The metatitanic acid particle size distribution was determined when the HTS concentration was 160 g L⁻¹, the STS concentration was 30 g L⁻¹, the microwave heating time was 60 s, the Fe/TiO₂ ratio was 0.3 and the H₂SO₄/TiO₂ ratio was 1.9.
ratios were over 90%. With the H₂SO₄/TiO₂ mass ratio increasing, the hydrolysis ratio dropped drastically. This tendency was similar to other TiO₂ manufacturing processes.⁴⁵,⁴⁸ At a low concentration of hydrolysis liquid of titanyl sulfate solution, the stability of the solution was poor. Adding the iron ions in the solution could promote ion hydration, and leading to a higher stability of the hydrolysis, which would benefit the hydrolysis reaction. Therefore, to get titanium dioxide with good pigment properties, a certain ion concentration was necessary to ensure the growth of the grains on the crystallization center.⁴⁹

A suitable H₂SO₄/TiO₂ mass ratio can also increase the stability of the hydrolysis liquors. However, since sulfuric acid is the product in the hydrolysis reaction, too high a concentration of sulfuric acid would result in a strong restraining effect of the sulfuric acid in the hydrolysis reaction. And it would lead to a low hydrolysis ratio and a small particle size.

The metatitanic acids obtained with different Fe/TiO₂ mass ratios were characterized as shown in Fig. 5. Although the mass ratio of Fe/TiO₂ affected the hydrolysis ratio little, it did affect

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Table 4   Effects of hydrolysis conditions⁵⁰

| No. | Seeds added amount [mass ratio, %] | Fe/TiO₂ | H₂SO₄/TiO₂ | Hydrolysis ratio (%) |
|-----|-----------------------------------|--------|------------|---------------------|
| 1   | 2.0                               | 0.0    | 1.9        | 94.4                |
| 2   | 2.0                               | 0.1    | 1.9        | 93.9                |
| 3   | 2.0                               | 0.2    | 1.9        | 94.4                |
| 4   | 2.0                               | 0.4    | 1.9        | 95.4                |
| 5   | 2.0                               | 0.3    | 2.0        | 94.3                |
| 6   | 2.0                               | 0.3    | 2.2        | 85.2                |
| 7   | 2.0                               | 0.3    | 2.4        | 63.2                |
| 8   | 2.0                               | 0.3    | 2.5        | 56.3                |
| 9   | 2.5                               | 0.3    | 1.9        | 95.1                |
| 10  | 1.5                               | 0.3    | 1.9        | 94.6                |
| 11  | 1.0                               | 0.3    | 1.9        | 92.1                |
| 12  | 0.5                               | 0.3    | 1.9        | 89.9                |

⁵⁰ The HTS concentration was 160 g L⁻¹, the hydrolysis temperature was 104 °C and hydrolysis time was 3.5 h. The seeds were prepared under STS concentration of 30 g L⁻¹, the microwave heating power was 800 W and the microwave heating time was 60 s.
the particle size distribution of the products. When Fe/TiO₂ was 0, the particle size distribution was narrower than the others. This may be caused by the iron ion concentration substantially affecting the morphology of metatitanic acid.⁴⁷

As shown in Fig. 6, the particle size distribution of the products was obviously affected by the mass ratio of H₂SO₄/TiO₂. Since H₂SO₄ was the product of the hydrolysis process, the hydrolysis process was restrained with a high initial H₂SO₄ concentration, and the crystals grew with difficulty. As a consequence, the smaller crystals were easier to aggregate, finally causing the metatitanic acid particle size distribution to widen. The hydrolysis particle changes along with the hydrolysis time are shown in Fig. 7. Overall, as the hydrolysis proceeds, the particle size distribution of metatitanic acid widens obviously while the particle sizes were almost the same. The seeds added were the same in these entries. And the particle size distribution grew remarkably on the high diameter side, and the height of the peaks became less as the hydrolysis time increased from 0.5 h to 3.5 h. At a hydrolysis time of 3.5 h, the hydrolysis ratio was just about 67.3% (as shown in Table 1, No. 7), and the particle size distribution of metatitanic acid was similar to the results in Fig. 3. This suggested the final size distribution could be further widened and the particle size would tend to high particle diameters.

As discussed above, the particle size of metatitanic acid seemed to be relevant to the hydrolysis process, which means that the seeds added in the hydrolysis should be of a consistent particle size and activity. On the contrary, the particle size distribution of the metatitanic acid broadened with hydrolysis proceeding, because of the particles growing. This microwave-

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Fig. 6  Particle size distributions of hydrolysis products with different H₂SO₄/TiO₂ mass ratios.

Fig. 7  The particle size distribution of metatitanic acid with different hydrolysis times. The experiments were carried out under the following conditions: STS concentration of 30 g L⁻¹, microwave heating time of 40 s, HTS concentration of 160 g L⁻¹, Fe/TiO₂ mass ratio of 0.3, H₂SO₄/TiO₂ mass ratio of 1.9, reaction temperature of 104 °C.

Fig. 8  XRD characterization for metatitanic acids produced by self-generating seeds and microwave-assisted seeds. (1A) Metatitanic acid produced by self-generating seeds. (1B) Metatitanic acid produced by microwave-assisted seeds. (2A) TiO₂ produced by self-generating seeds. (2B) TiO₂ produced by microwave-assisted seeds.
assisted seed preparation method was proved to apply to different kinds of hydrolysis liquid. And a uniform product with a narrow particle size distribution could also be ensured with these seeds.

3.3 Crystal transformation in calcination

External crystal seeds decide the particle size and properties of the hydrolysis product, metatitanic acid. The pigment TiO₂ is obtained by calcination of the hydrolysis metatitanic acid precursor, and the activity and properties significantly influence the pigment properties and also decide the crystal phases. TiO₂ obtained from the hydrolysis precursor in the sulfate process is normally anatase-type TiO₂. In order to produce rutile phase TiO₂ pigment, the precursor is often subjected to an elevated temperature so that the crystal transforms from anatase to rutile in the presence of a crystal transforming agent. In this work, the crystal transformation in the calcination process was investigated for metatitanic acid obtained by the hydrolysis in the presence of external crystal seed.

In this section, the metatitanic acid produced under the conditions of seed concentration of 30 g L⁻¹, mass ratio of Fe/TiO₂ of 0.3, and H₂SO₄/TiO₂ mass ratio of 1.9 was used to investigate the calcination process.

The hydrolysis samples obtained by using the microwave-assisted seeds as external crystal seeds were compared with the metatitanic acid products produced by self-generating seeds. XRD measurements showed that both metatitanic acid samples were anatase phase (as shown in Fig. 8, JCPDS 21-1272). Unlike commercial TiO₂, the sample with microwave-assisted seeds converted to rutile (JCPDS 21-1276) after being calcined at 850 °C. While the product from the self-generating seeds process was mainly still anatase.

Fig. 9 demonstrates the XRD profiles of hydrolysis samples (microwave-assisted seeds) after undergoing calcination at different temperatures. The metatitanic acid products produced by microwave-assisted seed processes can easily transform to rutile crystal phase.

To further confirm the morphology before and after calcination, the metatitanic acid particles and rutile products produced with this microwave process were characterized using SEM, and the results are shown in Fig. 10. The metatitanic acid particles were approximately 1–2 μm and of a narrow size distribution, which is consistent with the particle size analyzer results. The rutile particles are approximately uniform and of 100 nm in size, and could be considered to be uniform and small particles. This rutile particle size can be attributed to the narrow particle size distribution of metatitanic acid.

4. Conclusions

A novel microwave-assisted process to prepare seeds from dilute titanyl sulfate solution was developed for titanyl sulfate hydrolysis to produce anatase and rutile forms of TiO₂.

Use of microwaves could lead to uniform seeds of small particle size. The seeds from this new process were proved to have an equal stability and activity. With microwave energy...
increasing, the activity of the seeds increased, while the stability decreased. This would lead to a higher hydrolysis ratio.

This microwave-assisted seed preparation technology was proved to be effective under different hydrolysis conditions. The particle size of metatitanic acid products was small (about 1–2 μm), and the particle size distribution of the product was quite narrow and steady. The anatase product could easily transform to rutile (about 100 nm) through calcination at an unexpectedly low temperature. Henceforth, the production of rutile from the sulfuric acid process prepared without crystal transfer seeds at low temperature could be realized.

**Conflicts of interest**

There are no conflicts to declare.

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