Ultra - High Energy Cosmic Rays from decay of the Super Heavy Dark Matter Relics.

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I. INTRODUCTION

The origin of Ultra – High Energy Cosmic Rays (UHECR) with energy above the Greisen-Zatsepin-Kuzmin (GZK) cutoff, \( E_{GZK} \sim 10^{20} \) eV, is one of the most intriguing mysteries of the modern physics and astrophysics. After the pioneering papers \(^{[1]}\) and recent observations of the UHECR energy power spectra by AGASA \(^{[2]}\), Fly’s Eye \(^{[3]}\) and Haverah Park \(^{[4]}\), several possible mechanisms of the UHECR production were discussed (see reviews \(^{[5,6]}\)).

In this paper we consider the so-called Top-Down scenario of the UHECR creation which is associated with decays of Super Heavy Dark Matter (SHDM) particles with masses \( m_{\text{SHDM}} > 10^{12} \) GeV. This mechanism was for the first time suggested by Berezinsky, Kachelrieß and Vilenkin \(^{[7]}\) (see also \(^{[8]}\)) and now it seems to be a natural way of explaining the origin of UHECR with energies above the GZK cutoff.

Several kinds of SHDM particles which could be created in the early Universe are discussed in literature. Particles with masses of about one to two orders of magnitude larger than the typical mass of inflaton, \( m_{\phi} \sim 10^{13} \) GeV, could be very efficiently created at the preheating phase of inflation \(^{[9]}\). SHDM particles can also be related to topological defects, such as strings \(^{[10,11]}\), magnetic monopoles \(^{[12,13]}\), necklaces \(^{[14]}\) and vortons \(^{[15]}\).

The possible contribution of primordial black hole relics (PBHs) to the dark matter (DM) were discussed already in \(^{[16]}\) and \(^{[17]}\). Recently Dolgov, Naselsky and Novikov \(^{[18]}\) considered PBHs with masses \( M_{PBH} \sim 10^6 \) g as possible sources of the baryonic asymmetry and the high entropy of the Universe. They assume that remnants of such black holes with masses of about Planck mass survive up to now and form the SHDM relics. Mergers of these remnants within high density clumps creates more massive black holes, stimulates their explosive evaporation and could produce ultra-high energy particles observed as rare UHECRs.

This discussion shows that, in the framework of the Top-Down scenario, the UHECR can be related to various kinds of SHDM particles with masses \( 10^{12} \leq m_X \leq 10^{19} \) GeV. (Below by X we denote all possible types of SHDM).

Now the possible energy losses of the UHECR are well established \(^{[19]}\) and observational predictions of the Top-Down scenario of the UHECR creation crucially depend upon unknown factors such as the mass of the SHDM particles, energy spectrum and composition of decay products. It is commonly believed, that the observed UHECR spectrum at both \( E \leq E_{GZK} \) and \( E \geq E_{GZK} \) is dominated mainly by local sources and it simply reproduces the spectra of injected protons. However, at energies \( E \sim E_{GZK} \), the complex shape of observed UHECR fluxes shows that it can be more sensitive to extragalactic component of high energy protons and, so, can depend upon the unknown factors mentioned above. Detailed investigation of the spectrum and anisotropy of UHECR in the range \( E/E_{GZK} \geq 0.1 \) can discriminate between discussed versions of the Top-Down models and restrict some parameters of the SHDM particles and the process of proton creation.

As is commonly believed, decays of SHDM particles into the high energy protons, photons, electron-positron pairs and neutrinos occurs through the production of quark-antiquark pairs \( (X \to q \bar{q}) \), which rapidly hadronize and generate two jets and transform the en-
ergy into pions (~95%) and hadrons (~5%) \cite{21}. It can be expected that later most of that energy is transformed into high energy photons and neutrinos with the energy spectrum \( S(E) \propto E^{-1.5} \), at \( E \ll M_X \) \cite{21}. Similar spectrum for the hadronic component is also expected. This means that, for such decays of SHDM particles with \( 10^{12} < m_X < 10^{19} \) GeV, the UHECR with energies \( E > 10^{20} \) eV are dominated by photons and neutrinos \cite{21}. This conclusion can be tested with further observations of the UHECR fluxes at \( E > 10^{20} \) eV.

Other spectra of protons generated by decays of SHDM particles are also discussed. In particular, such spectrum can be similar to Gaussian or \( \delta \)-function centered at \( E_X \sim m_X \gg 10^{20} \) eV. In this case the spectrum of protons created by nearby sources will be also similar to the same \( \delta \)-function while the spectrum of the extragalactic component is \( \propto E^{-1} \) at both \( E < E_GZK \) and \( E > E_GZK \) and is consistent with the observed one at \( E \sim E_GZK \).

Recently Berezinsky and Kachelrieß \cite{13} discussed Monte Carlo simulations of the jet fragmentation in SUSY- QCD. They found that the spectrum of injected protons can be well fitted to log-normal distribution. Farrar and Piran \cite{23} discussed the spectrum of injected protons \( S(E) \propto E^{-\alpha} \), with \( 0 < \alpha \leq 1 \) in the Top-Down model of the UHECR origin. We show that, for such spectra, the flux of extragalactic protons at \( E \sim E_GZK \) is also consistent with the observed one.

Another important factor is the observed anisotropy of the UHECR distribution over the sky. As was discussed by Berezinsky et al. \cite{8}, both CDM and SHDM particles are clustered within galactic halos and their decays inevitably generate some anisotropy. In particular, if the contribution of Galactic sources dominates we will see an anisotropy of the UHECR due to our asymmetric position in the Galaxy. In contrast, the extragalactic component of UHECRs is averaged over the volume with a size \( \geq 50 \) Mpc and its angular distribution is almost isotropic. The contributions of closest galaxies and the Local Supercluster of galaxies could also be observed.

The relative contributions of Galactic and extragalactic UHECRs sources depend upon many unknown factors such as the size of galactic halo, overdensity and spatial distribution of SHDM particles within the halo \cite{8}. However, for larger energy of injection, \( E_{inj} \geq 10^{4} - 10^{5} E_GZK \), and for Gaussian, log-normal and power spectra of injected protons with \( \alpha \leq 0.6 \), the contribution of extragalactic UHECRs dominates at \( E \sim E_GZK \), whereas at both less and larger energies the contribution of galactic sources becomes more important. This means that the anisotropy of angular distribution of UHECRs depends upon their energy and, for the Top-Down model with spectra under discussion, it is minimal at \( E \sim E_GZK \).

In this paper we recalculate the contribution of the extragalactic component of UHECR for different life – time, masses of the SHDM particles \( 10^{12} \) GeV \( \leq m_X \leq 10^{19} \) GeV, and spectra of injected proton. We show that the relative contributions of galactic and extragalactic components of high energy protons depend upon these factors. For the most interesting models, the extragalactic component is found to be dominant at \( E \sim E_GZK \) and the expected flux is well consistent with observations. The expected angular distribution on the sky of observed UHECR flux depends upon the energy of protons near the GZK cutoff and its variations should be considered as an important test for the Top-Down models.

Some cosmological manifestations of decays of SHDM particles can also be observed. In particular, decays of SHDM particles with masses \( m_X \sim 10^{19} \) GeV can delay the recombination of hydrogen at redshifts \( z \sim 1000 \). This inference is especially important for discussion of the Cosmic Microwave Background (CMB) anisotropy and polarization power spectra. The same decays can increase the hydrogen ionization at smaller redshifts and accelerate the formation of first population of stars and galaxies. These manifestations can be tested with both available and future measurements of the CMB anisotropy and polarization.

The paper is organized as follows. In section 2 we discuss the spectra of extragalactic protons for different spectra of injected protons, in section 3 the combined flux of galactic and extragalactic sources is compared with observations. In section 4 we discuss the possible delay of hydrogen recombination due to decays of the SHDM particles. Main results are discussed in section 4.

II. EXPECTED SPECTRUM OF HIGH ENERGY PROTONS

In this paper we use the continual energy loss (CEL) approximation and describe the evolution of the number density of high energy extragalactic protons by the following equation \cite{6}:

\[
\frac{dN(E,t)}{dt} + 3H(t)N + \frac{\partial}{\partial E} \left( N \frac{dE}{dt} \right) = I(E,t),
\]

\[
\frac{dE}{dt} = -H + H_0 \beta(E), \quad \beta(E) = \beta_\pi(E) + \beta_\gamma(E),
\]

\[
I = \omega_p \frac{n_0}{70} (1 + z)^3 S(E), \quad H = -\frac{1}{1+z} \frac{dz}{dt} = H_0 (1 + z)^{3/2},
\]

where \( E \) and \( N(E,t) \) are the energy and number density of protons per unit of energy, \( H(t) \) is the Hubble constant, \( H_0 = 100 \) km/s/Mpc = 75 km/s/Mpc, \( z \) is a redshift, the functions \( I(E,t) \) and \( S(E) \) characterize the intensity and spectrum of injected protons, \( \omega_p n_0 / 70 \) is the intensity of proton production at \( z = 0 \), functions \( \beta_\pi(E) \) and \( \beta_\gamma(E) \) describe the proton energy losses due to electron – positron pairs and photo-pions production and \( \omega_\pi \sim 0.05 \) is the fraction of protons in the SHDM particles decay.
The general solution of equation (1) is
\[
N_{ee}(E_0, t_0) = \int_1^\infty \frac{dx}{x^4 E_0} \left( 1 + \frac{\beta(E)}{E} \right) H(x) = \\
\frac{\omega_p n_0}{H_0 t_0} \int_1^\infty \frac{dx}{x^{5/2} E_0} \left( 1 + \frac{\beta(E)}{E} \right) S(E(x)),
\]
where \( E = E(x), \ E_0 = E(z = 0), t_0 = t(z = 0) \). This means that, in fact, the observed flux of extragalactic UHECRs depends upon the functions \( \beta(E) \) and \( S(E) \).

\[
\beta(1 + z)^{3} \kappa, \ (1 + z) \epsilon \geq 1,
\]
\[
\beta(1 + z)^{3} \kappa \epsilon^{p_1}, \ 1 \geq (1 + z) \epsilon \geq \epsilon_1,
\]
\[
\beta(1 + z)^{3} \kappa \epsilon^{p_2} \epsilon_1^{p_1-p_2}, \ \epsilon_1 \geq (1 + z) \epsilon \geq \epsilon_2,
\]
\[
\beta(1 + z)^{3} \kappa \epsilon^{p_3} \epsilon_1^{p_1-p_2} \epsilon_2^{p_2-p_3}, \ \epsilon_2 \geq (1 + z) \epsilon, \ (1 + z) \epsilon \geq 0.6, \ \epsilon_2 \approx 0.27, \ p_1 \approx 1.3, \ p_2 \approx 4, \ p_3 \approx 0.3,
\]
\[
\epsilon = E/E_{GZK}, \ E_{GZK} \approx 1.5 \cdot 10^{20} \text{eV},
\]
\[
\kappa = \frac{cH_0^{-1}}{D(E_{GZK})} \approx 160, \ D(E_{GZK}) = 25 \text{Mpc}.
\]

where the redshift dependence of density and temperature of CMB is taken into account. The function \( \beta(E_{GZK})/\beta(E) = D(E)/D(E_{GZK}) \) is plotted in Fig. 1.

For \( E \ll E_{GZK} \), the energy losses due to \( e^+e^- \) pair production dominates (for review, see [21]) and
\[
\beta_e \approx 0.005(1 + z)^3 \kappa. \quad (8)
\]

For these functions \( \beta(E) \), the redshifts variations of the proton energy can be found analytically as follows:
\[
E(z_2) = E(z_1) \frac{1 + z_2}{1 + z_1} G_e(z_1, z_2), \ \beta(E) = \kappa = \text{const}, \quad (9)
\]
\[
G_e(z_1, z_2) = \exp\left( \frac{2}{3} \kappa [(1 + z_2)^{3/2} - (1 + z_1)^{3/2}] \right),
\]
\[
E(z_2) = E(z_1) \frac{1 + z_2}{1 + z_1} G_p(z_1, z_2), \ \beta(E) = \kappa e^p, \quad (10)
\]
\[
G_p(z_1, z_2) = 1 - \frac{\kappa p \epsilon^p(z_1)}{p + 3/2} \left( \frac{1 + z_2}{1 + z_1} \right)^{p + 3/2} - 1.
\]

For \( p \to 0 \), \( G_p(z_1, z_2) \to G_e(z_1, z_2) \) and the expression [11] becomes identical to [10].

B. Galactic and extragalactic protons

The high concentration of the SHDM particles within the halo of Galaxy generates the galactic component of UHECRs, \( N_{gal} \). Its spectrum reproduces the spectrum of generated protons. For the popular King’s profile of density distribution in halo,
\[
\rho(r) = \rho_c (1 + r^2/\rho_c^2)^{-3/2},
\]
with the size of the core \( r_g \approx 10 \text{kpc} \) (see, e.g., [24]), the relative contribution of galactic and extragalactic components can be roughly estimated as follows:
\[
N_{gal}(E) = \frac{\omega_p n_0 r_g}{\rho_c H_0 t_0} \delta_g S(E) = \zeta_{gal} \frac{\omega_p n_0}{H_0 t_0} S(E), \quad (12)
\]
\[
\zeta_{gal} \sim \frac{H_0 r_g}{c} \delta_g = 0.3 \frac{r_g}{10 \text{kpc}} \delta_g 10^5.
\]

where \( \delta_g \) is the overdensity of the core above the mean density of DM component. More detailed analysis [11] extends the range of possible ratio of galactic to extragalactic components up to \( \zeta_{gal} \sim 30 \sim 50 \). Further on for comparison of galactic and extragalactic fluxes, we will take \( \zeta_{gal} \sim 10 \).
1. Spectra of extragalactic protons

Both the observed fluxes and relative contributions of galactic and extragalactic components depend upon the spectrum of injected protons, \( S(E) \). To illustrate this dependence we consider the normalized power spectra with exponents \( \alpha \geq 1 \) and \( \alpha \leq 1 \) and the log-normal spectrum proposed in [14].

Spectrum with \( \alpha = 1.5 > 1 \) and \( E_{\text{min}} \ll E \leq E_{\text{inj}} \),

\[
S_{\text{pw}}(E) = \frac{\alpha - 1}{E_{\text{inj}}} \left( \frac{E}{E_{\text{inj}}} \right)^{-\alpha} \left( 1 - \frac{E}{E_{\text{inj}}} \right)^2,
\]

is usually used to describe the decay of particles with moderate masses. It is model dependent and its applicability to the decay of extremely massive X-particles is in question (see, e.g., discussion in [13]). For such spectrum, using [3], we obtain

\[
N_{\text{ex}} = \frac{\omega_{\text{inj}} \mu - 1}{H_0 \tau_0} \left( \frac{E_0}{E_{\text{inj}}} \right)^{-\alpha} \nu(E_0, \alpha).
\]

The dimensionless function \( \nu(E_0, \alpha) \) weakly depends upon \( \alpha \) and describes how the flux of extragalactic protons varies with energy at \( E_0 \sim E_{\text{GZK}} \). Numerically, \( \nu(E_{\text{GZK}}, 1.5) \approx 10^{-2} \).

As is seen from [13] in this case both spectra of extragalactic and galactic protons are similar and the contribution of extragalactic component to the observed fluxes of UHECR is small, because \( \nu \ll \zeta_{\text{gal}} \).

Spectra of injected protons with \( \alpha \leq 1 \),

\[
S_{\text{pw}}(E) = \frac{c(\alpha)}{E_{\text{inj}}} \left( \frac{E}{E_{\text{inj}}} \right)^{-\alpha} \left( 1 - \frac{E}{E_{\text{inj}}} \right)^2,
\]

\[
c(\alpha) = 0.5(1 - \alpha)(2 - \alpha)(3 - \alpha),
\]

seem to be more promising. For such spectra with \( \alpha \leq 0.6 \) and \( E_{\text{inj}} \geq 10^8 E_{\text{GZK}} \), we have almost universal spectrum of extragalactic protons,

\[
N_{\text{ex}}(E_0) = \frac{\omega_{\text{inj}} \mu - 1}{H_0 \tau_0} E_0^{-1} \mu(E_0, E_{\text{inj}}, \alpha),
\]

\[
\mu(E_{\text{GZK}}, E_{\text{inj}}, \alpha) \approx (0.5 - 1.5) \cdot 10^{-2}.
\]

for models with large and short life – time of the SHDM particles, respectively. Dimensionless function \( \mu(E_0, \alpha) \) weakly depends upon \( E_{\text{inj}} \) and \( \alpha \) and describes variations of the flux of extragalactic protons with energy at \( E_0 \sim E_{\text{GZK}} \). For such spectra of injected protons galactic component dominates only at high energy when

\[
\left( \frac{E_0}{E_{\text{inj}}} \right)^{1-\alpha} \geq \frac{\mu(E_0, E_{\text{inj}}, \alpha)}{c(\alpha)\zeta_{\text{gal}}}.
\]

We consider also the log-normal spectra of injected protons recently proposed in [13] (see also [8]),

\[
S_{\text{inj}}(E) = \frac{1}{\sqrt{2\pi} E\sigma_{\text{inj}}} \exp \left( -\frac{\ln^2(E/E_{\text{inj}})}{2\sigma_{\text{inj}}^2} \right),
\]

with \( \sigma_{\text{inj}} = 3 - 7 \) and the same two energies of injection as above. In this case the spectrum of extragalactic protons is also almost universal and similar to [17] with a similar function \( \mu(E_0, E_{\text{inj}}, \sigma_{\text{inj}}) \). For such spectrum, the contribution of galactic sources is shifted to energy \( E_0 \sim E_{\text{inj}} \exp(-\sigma_{\text{inj}}) \) and dominates only at high energy when

\[
\ln^2 \left( \frac{E_0}{E_{\text{inj}}} \right) \leq 2\sigma_{\text{inj}}^2 \ln \left( \frac{\zeta_{\text{gal}}}{\sqrt{2\mu\sigma_{\text{inj}}}} \right).
\]

2. Cumulative fluxes of galactic and extragalactic protons

As is seen from [13] for the spectra of injected protons with \( \alpha \geq 1 \) the contribution of galactic protons dominates at all energies for \( \zeta_{\text{gal}} \geq \nu(E_{\text{GZK}}, \alpha) \sim 10^{-2} \). In contrast, for both spectra with power index \( \alpha \leq 1 \) and log-normal spectra of injected protons, the galactic component dominates only at higher energies as is given by [15] and [24].

Comparison of the cumulative fluxes of these components shows that, for both spectra (16) and (20), the extragalactic component dominates when

\[
\zeta_{\text{gal}} \leq \mu(E_{\text{GZK}}) \ln(E_{\text{inj}}/E_{\text{GZK}}).
\]

Due to the universal spectrum of extragalactic protons [13], this estimate does not depend upon detailed characteristics of spectra of injected protons and shows that even for \( E_{\text{inj}} \sim 10^8 E_{\text{GZK}} \) the cumulative extragalactic component dominates only for \( \zeta_{\text{gal}} \leq 0.1 \sim 0.3 \), for large and short life – time of the SHDM particles. These values are close to the estimate [13] but are less then those discussed in [3]. This means that, for both spectra (16) and (21), the domination of galactic component could be expected at \( E \sim E_{\text{inj}} \gg E_{\text{GZK}} \).

III. EXPECTED FLUX OF PROTONS FOR TOP-DOWN MODELS

Here we consider the Top–Down models for two injection energies, \( E_{\text{inj}} = 10^2 E_{\text{GZK}} \) and \( E_{\text{inj}} = 10^8 E_{\text{GZK}} \). The first model is related to decays of SHDM particles with moderate masses often discussed in literature (see, e.g., [16]). The second model describes the decay of ultra massive particles such as, for example, explosive evaporation of black hole remnants discussed in Dolgov, Naselsky & Novikov [21].

To illustrate the influence of the life – time of the SHDM particles, \( \tau_0 \), we consider two models, one with \( \tau_0 \) larger than the age of the Universe, \( T_U \sim H_0^{-1} \), and other with \( \tau_0 \approx 0.1 T_U \).
The normalized expected fluxes of UHE protons,

\[ F(\varepsilon_0) = \frac{dJ(E_0)}{dE_0} \frac{E_0^3}{10^{24} \text{eV}^2 \text{m}^{-2} \text{s}^{-1} \text{cm}^{-2}} \]  \tag{23}

are plotted in Figs. 2 - 5 versus \( \varepsilon_0 = E_0/E_{\text{GZK}} \) together with available observational data. We show the fluxes of extragalactic component alone and combined fluxes for extragalactic and galactic components for \( \zeta_{\text{gal}} = 10 \).

![Graph showing expected fluxes of UHE protons](image)

**FIG. 2.** The functions \( F(\varepsilon_0) \) versus \( \varepsilon_0 = E_0/E_{\text{GZK}} \) are plotted for long-lived SHDM particles with \( \tau_0 \gg T_U \), \( E_{\text{inj}}/E_{\text{GZK}} = 10^2 \), and power spectra of injected protons with \( \alpha = 1.5 \) (long dashed line), \( \alpha = 0.5 \) (solid line), and \( \alpha = 0.25 \) (dashed line). Thin lines show the contribution of extragalactic component alone, thick lines show the contribution of extragalactic and galactic sources for \( \zeta_{\text{gal}} = 10 \). The observed fluxes are plotted by points. For comparison, the flux \( dJ/dE_0 \propto E_0^{-1} \) is plotted by dotted line.

**A. Models with power spectra of injected protons**

As was noted above, for power spectra \( \alpha \equiv \beta \) with larger exponent \( \alpha = 1.5 \geq 1 \), the contribution of extragalactic component, \( N_{\text{ex}}(E_0) \), weakly depends upon the energy of injection and is negligible in comparison with the contribution of the galactic component. These results are a natural consequence of predominant generation of lower energy protons in such models. Of course, for suitable choice of decay rate, \( n_0/\tau_0 \), the galactic component can explain the observed growth of flux at \( E \geq E_{\text{GZK}} \).

1. **Models with \( \alpha \leq 1 \) and larger life-time of the SHDM particles, \( \tau_0 \gg T_U \)**

For models with smaller exponents, \( \alpha = 0.5 \) and 0.25, and moderate energy of injection, \( E_{\text{inj}} = 10^2 E_{\text{GZK}} \), plotted in Fig. 2, the resulting flux is sensitive to the contribution of galactic component and, for the most interesting energies \( E_0 \geq 0.2 - 0.3 E_{\text{GZK}} \), the impact of extragalactic component becomes noticeable only for \( \zeta_{\text{gal}} \leq 1 \). These results agree with approximate estimates \( \| \).

For models with high energy of injection, \( E_{\text{inj}} = 10^8 E_{\text{GZK}} \), and with smaller exponents, \( \alpha = 0.5 \) and 0.25, the expected spectrum of extragalactic component is similar to \( (17) \), and the resulting flux is weakly sensitive to the contribution of the galactic component. For the most interesting energies, \( E_0 \sim E_{\text{GZK}} \), the extragalactic component dominates, at least for \( \zeta_{\text{gal}} \leq 30 \).

Results plotted in Fig. 3 show that, for suitable decay rate,

\[ \omega_p n_0/\tau_0 \approx 10^{-46} \text{cm}^{-3} \text{s}^{-1}, \]  \tag{24}

such models reproduce quite well the observed fluxes of UHECR with energies \( E \geq 0.1 E_{\text{GZK}} \).

![Graph showing expected fluxes of UHE protons](image)

**FIG. 3.** The functions \( F(\varepsilon_0) \) versus \( \varepsilon_0 = E_0/E_{\text{GZK}} \) are plotted for long-lived SHDM particles with \( \tau_0 \gg T_U \), \( E_{\text{inj}}/E_{\text{GZK}} = 10^5 \), and power spectra of injected protons with \( \alpha = 1.5 \) (long dashed line), \( \alpha = 0.5 \) (solid line). Thin lines show the contribution of extragalactic component alone, thick lines show the contribution of extragalactic and galactic sources, for \( \zeta_{\text{gal}} = 10 \). The observed fluxes are plotted by points. For comparison, the flux \( dJ/dE_0 \propto E_0^{-1} \) is plotted by dotted line.

**2. Models with shorter life-time of the SHDM particles**

In models with shorter life-time of the SHDM particles, \( \tau_0 \sim 0.125 T_U \), the number density of SHDM particles rapidly decreases with time due to their progressive decays what, in turn, increases the contribution of extragalactic component for \( 0.1 \leq E_0/E_{\text{GZK}} \leq 1 \). In spite of this, for models with moderate energy of injection,
$E_{inj} = 10^2 E_{GZK}$, this factor cannot essentially amplify the contribution of extragalactic component and it becomes noticeable only for $\zeta_{gal} < 10$.

However, for models with ultra - high energy of injection, $E_{inj} = 10^8 E_{GZK}$, and smaller exponents, $\alpha = 0.5$ and $\alpha = 0.25$, results plotted in Fig. 4 for $\tau_0 = 0.125 T_U$, demonstrate that, for $E_0 \geq 0.06 E_{GZK}$, the extragalactic component dominates. For the decay rate

$$\frac{\omega_{p} n_0}{\tau_0} \approx 0.3 \cdot 10^{-45} \text{cm}^{-3} \text{s}^{-1}, \; n_0 \sim \omega_{p}^{-1} 10^{-30} \text{cm}^{-3},$$

(25)

it reproduces quite well the observed flux of UHECR for energy $E \geq 0.06 E_{GZK}$. If SHDMs are identified with primordial black holes with $M_{pbh} \sim 10^{-5} g$ then the mean densities of SHDMs at $z = 0$ and at $z \gg 1$ are

$$\rho(0) \sim \omega_p^{-1} 10^{-35} g \text{ cm}^{-3},$$

(26)

$$\rho(z) (1+z)^{-2} \sim \omega_p^{-1} (10^{-31} - 10^{-32}) g \text{ cm}^{-3} \leq \rho_{cr},$$

(27)

respectively.

![FIG. 4. The functions $F(\epsilon_0)$ (23) versus $\epsilon_0 = E/E_{GZK}$ are plotted for short-lived SHDM particles with $\tau_0 = 0.125 T_U$, $E_{inj}/E_{GZK} = 10^8$, and power spectra of injected protons with $\alpha = 1.5$ (long dashed line), $\alpha = 0.5$ (solid line). Thin lines show the contribution of extragalactic component alone, thick lines show the contribution of extragalactic and galactic sources, for $\zeta_{gal} = 10$. The observed fluxes are plotted by points. For comparison, the flux $dJ/dE_0 \propto E_0^{-1}$ is plotted by dotted line.](image)

**B. Models with log-normal spectra of injected protons**

For log-normal spectra of injected protons, $S_{inj}$, (20), with moderate dispersions $\sigma_{inj} = 5$ and energies of decays $E_{inj} = 10^2 E_{GZK}$ and $E_{inj} = 10^8 E_{GZK}$, the resulting fluxes of UHECRs, for $\zeta_{gal} = 10$, are plotted in Fig. 5. For models with larger $E_{inj}$, the expected flux at $E_0 \sim E_{GZK}$ is dominated by the extragalactic component and reproduces the observed flux variations. In contrast, for models with smaller $E_{inj}$, the expected flux is dominated by the galactic component and is far from the observed one. The contribution of galactic sources at $E_0 \sim E_{GZK}$ depends upon $\zeta_{gal}$ and rapidly decreases for larger $E_{inj}$ and smaller $\sigma_{inj}$.

At $E \leq E_{GZK}$ the extragalactic flux is more sensitive to the life – time of SHDM particles. As is seen from Fig. 5 for the decay rate of SHDM particles (24) and longer life – time, $\tau_0 \gg T_U$, the resulting fluxes, for $E_0 \geq 0.3 E_{GZK}$, describe quite well the observations. For shorter life – time, $\tau_0 \sim 0.1 T_U$, and the decay rate of SHDM particles (24), this fluxes reproduce well the observations up to $E_0 \sim 0.06 E_{GZK}$.

![FIG. 5. The functions $F(\epsilon_0)$ (23) versus $\epsilon_0 = E/E_{GZK}$ are plotted for log-normal spectra of injected protons with the life – time $\tau_0 \gg T_U$, $\sigma_{inj} = 5$ for $E_{inj} = 10^8 E_{GZK}$ (thin solid line) and $E_{inj} = 10^5 E_{GZK}$ (thick solid line). For $\tau_0 \approx 0.125 T_U$, $E_{inj} = 10^8 E_{GZK}$, the same function is plotted for $\sigma_{inj} = 5$ (dashed line) and $\sigma_{inj} = 7$ (long dashed line). The observed fluxes are plotted by points.](image)

**IV. SOME COSMOLOGICAL MANIFESTATIONS OF DECAYS OF SHDM PARTICLES**

The injection of energy due to decays of SHDM particles during the "dark ages", at redshifts $10^3 \geq z \geq 10$, leads also to interesting consequences some of which can be tested with available and/or future observations. Such consequences were recently discussed by Peebles, Seager and Hu (23) in the framework of a simple toy model. Here we repeat this analysis using results obtained above.
The decays of SHDM particles produce, among others, many high energy photons and electron – positron pairs which, after reduction of their energy in electromagnetic cascades, are converted into $Ly –\alpha$ and $Ly –\gamma$ photons with energies $E_\alpha = 10.2 eV$ and $E_\gamma = 13.6 eV$, respectively. The efficiency of such conversion is small due to high complexity of these cascades. To avoid many assumptions required for discussion of the final intensity and spectrum of photons at energy of interest we will assume, following [25], that the decays of SHDM particles lead to creation of $Ly –\gamma$ and $Ly –\alpha$ photons with a rate

$$\frac{dn_{ph}}{dt} \approx \varepsilon_{ph} \frac{E_{inj} n_0}{\tau_0} \approx \left(\frac{1 + z}{1000}\right)^3 \cdot 10^{-10} \frac{\varepsilon_{ph}}{cm^3 s}, \quad (28)$$

where, for numerical estimates, we use $E_{inj} = 10^8 E_{GZK} \approx 10^{28}$ eV, the decay rate $n_0/\tau_0 = 10^{-46} cm^{-3}s^{-1}$, and $\varepsilon_{ph} \ll 1$ characterizes the unknown efficiency of energy transformation to $Ly –\gamma$ and $Ly –\alpha$ photons.

Comparing the rate of photons creation (28) with the rates discussed in [23],

$$\frac{dn_\alpha}{dt} = \varepsilon_{\alpha} n_H H \approx 2.5 \cdot 10^{-14} \left(\frac{1 + z}{1000}\right)^{9/2} \frac{\varepsilon_{\alpha}}{cm^3 s}, \quad (29)$$

we see that, for $\varepsilon_{\alpha} \sim 1 – 10$ and correspondingly for

$$\varepsilon_{ph} \sim 3 \cdot 10^{-4} \varepsilon_{\alpha} \sim 10^{-4} – 10^{-3}, \quad (30)$$

the impact of discussed decays of SHDM particles effectively delays the recombination of hydrogen and leads to measurable distortions of the observed spectra of CMB fluctuations at angular wave numbers $l \geq 100 – 200$ (see detailed discussion in [23]).

For shorter life – time of SHDM particles, $\tau_0 \approx 0.125 T_s$, the decay rate at redshifts $z \geq 10$ increases by about a factor of $10^3$ in comparison with (28) and wider range of $E_{inj}$ and $\varepsilon_{ph}$ can also be considered. The effect of the impact of $\omega_p$ omitted in (28) will also reinforce these estimates.

At smaller redshifts, $z \leq 500$, generated $Ly –\gamma$ photons partly ionize neutral hydrogen. For small ionization degree of hydrogen, $x_H \leq 1$, all $Ly –\gamma$ photons are rapidly absorbed and $x_H$ can be found from the equilibrium equation which describes the conservation of number of electrons and $Ly –\gamma$ photons together,

$$\frac{dn_{ph}}{dt} = \alpha_{rec}^s n_e n_p = \alpha_{rec}^p (n_b)^2 x_H^2 \quad (31)$$

where $\alpha_{rec}^s \approx 2 \cdot 10^{-13} (T/10^4 K)$ is the recombination coefficient for states with the principal quantum number $n \geq 2$, $T/10^4 K \approx 0.03 [(1 + z)/100]^3$ is the temperature of hydrogen under the condition of small ionization, $(n_b) \approx 0.24 (\Omega_b h^2/0.02) [(1 + z)/100]^3$ is the mean number density of baryons, and $n_p = n_e = x_H (n_b)$. For simplicity, we neglected here the contribution of helium.

As follows from Eqs. (28) and (31), the expected degree of hydrogen ionization is

$$x_H \approx \varepsilon_{ph} \left(\frac{1 + z}{100}\right)^{-3/4}. \quad (32)$$

For $\varepsilon_{ph} \geq 10^{-6}$, this degree is higher than the degree of remaining hydrogen ionization after recombination, $x_H \sim 10^{-3}$. For shorter life – time of SHDM particles, $\tau_0 \approx 0.125 T_s$, the decay rate at redshifts of interest grows by about a factor of $10^3$ and increases the ionization degree up to

$$x_H \sim \sqrt{10^3 \varepsilon_{ph}} \left(\frac{1 + z}{100}\right)^{-3/4}, \quad (33)$$

that again essentially extends the range of acceptable $E_{inj}$ and $\varepsilon_{ph}$.

The considered growth of $x_H$, at redshifts $z \leq 500$, does not increase significantly the optical depth for Thompson scattering, $\tau_T$, because

$$\frac{d\tau_T}{dz} \propto x_H (1 + z)^{-3/2}.$$ 

So, it does not amplify perturbations of the observed spectra of CMB as compared with distortions generated at redshifts $z \approx 1000$. But this growth essentially accelerates the creation of molecules $H_2$ and therefore formation and cooling of first galaxies.

These results were obtained when the extragalactic component of UHECR, discussed in Sec. III, dominates. These estimates can be also repeated for decays of more massive SHDM particles and usually discussed spectra of injected protons, with $\alpha = 1.5$ and $n_0/\tau_0 \sim 10^{-46} cm^{-3}s^{-1}$.

V. SUMMARY AND DISCUSSION

Available information about possible properties of SHDM particles and, in particular, about their life – time, energy and spectra of injected protons is now very limited, and, in fact, the analysis of UHECR can be considered as an experimental test for particle interactions at ultra – high energy. Results obtained in previous Sections show that under quite natural assumptions about the energy, life-time and spectrum of injected protons, a reasonable explanation of the observed fluxes of UHECR can be achieved. The CEL approximation used in this paper describes quite well the expected fluxes at $E \leq E_{GZK}$ but, for larger energies, the observed fluxes can be essentially distorted due to random character of energy losses above the GZK cutoff [23].

For both log-normal and power spectra of injected protons, $S_{inj}$ [20] and $S_{pcu}$ [11], with $E_{inj} \geq 10^5 E_{GZK}$ and $\alpha \leq 1$, and for suitable intensity of proton creation and life – time of SHDM particles, our results are consistent
with the observed fluxes for $E_0 \geq 0.06E_{GZK}$. They demonstrate that, for $E_0 \sim E_{GZK}$, the observed flux of UHECR can be mainly related to the extragalactic component. For such spectra of injected protons, the expected flux is found to be moderately sensitive to assumptions about the galactic sources, the energy of injection for $E_{inj} \geq 10^5E_{GZK}$ and to values of $\alpha \leq 0.6$ and $\sigma_{inj} \leq 10$ for power and log-normal spectra, respectively. In contrast, for the models with power spectra and $\alpha \geq 1$ [4], and for models with smaller energy of injection, $E_{inj} \sim 10^2 - 10^3E_{GZK}$, the contribution of extragalactic component of UHECR is small, the galactic component dominates and the observed fluxes cannot be reproduced.

For simplicity and due to qualitative character of our analysis, we consider the CDM dominated flat cosmological model only. Evidently, these results can be recalculated in the same manner for other cosmological models and, in particular, for the most popular $\Lambda$CDM flat model. Of course, for such cosmological models some of the parameters used here will be changed. However, even for such models the main qualitative results concerning the influence of the life – time, mass and spectra of injected protons will remain.

B. Cosmological manifestations of decays of SHDM particles

The discussed cosmological manifestations of the Top-Down model of UHECR generation provide an indirect test of this model. As is seen from evaluations given in Sec. IV for the high masses of SHDM particles and energy of injection $E_{inj}/E_{GZK} \sim 10^8$, the effective delay of the cosmological recombination is possible for reasonable values of efficiency of creation of Layman photons. For models with decays of vortons, necklaces and other particles with $E_{inj}/E_{GZK} \ll 10^8$ these cosmological manifestations are negligible.

The expected distortions of CMB fluctuations due to delayed recombination can be directly tested with the available modern balloon-born experiments (MAXIMA-1 [26] and BOOMERANG [27]) and future – MAP and PLANCK satellite missions – by measuring the CMB anisotropy and polarization power spectra. These problems will be discussed elsewhere.

C. Expected composition of UHECR and restrictions of the Top–Down models

Special problem is the composition of expected UHECRs. As is well known, decay products are dominated by pions, photons and neutrinos while high energy protons make up only small part of these products. Therefore in the Top–Down models the observed flux of protons is accompanied by noticeable flux of high energy photons, electron - positron pairs and neutrinos. Probable energy losses of neutrinos are small, they are concentrated at $E \sim E_{inj} \gg E_{GZK}$ and could be responsible only for relatively rare observed events. But the comparison of expected and observed fluxes of high energy photons restricts some properties of SHDM particles and the Top–Down model as a whole (28).

The models under consideration predict the creation of high energy photons with $E \sim E_{inj} \gg E_{GZK}$. The
possible evolution of such photons is quite uncertain as it depends upon unknown factors such as the extragalactic magnetic field and properties of radio background. For photons with $E_p \gg E_{\text{GZK}}$, the free path, $D_\gamma \sim 100(1 + z)^{-3}\text{Mpc}$, is, probably, defined by the process of double pair production in the CMB photons, $\gamma\gamma_b \to e^+e^-e^+e^-$, which leads to formation of less energy photons in electromagnetic cascades. For photons with $E_\gamma \sim E_{\text{GZK}}$, the free path, $D_\gamma \sim 1\text{Mpc}(E/E_{\text{GZK}})^{-2}$ is defined in main by their interaction with a badly known radio background.

The flux and spectrum of the extragalactic component of photons differ from those expected for the protons. They depend upon the adopted life-time of the SHDM particles, properties of the electromagnetic cascades and radio background, and other factors. This complicated problem requires special detailed discussion.

However, estimates of the photon free–path show that, for decays of the SHDM particles, the galactic component is dominated by photons with the spectrum of injection. The cumulative contribution of the photons is more then the cumulative contribution of the protons by a factor of $\sim \omega_\gamma^{-1} \gg 1$. This means that even for models under consideration the cumulative observed flux of UHECRs at energy $E \geq E_{\text{GZK}}$ is also dominated by galactic component of photons with $E \sim E_{\text{inj}} \gg E_{\text{GZK}}$. This conclusion follows from quite general arguments and, in fact, the discrimination of high energy photon component of UHECRs can be considered as the crucial test for the Top–Down models.

Of course, the registration of such photons and the discrimination between photons with $E \gg E_{\text{GZK}}$ and protons with $E \sim E_{\text{GZK}}$ is special observational problem (see, e.g., [34]). Thus, recently published restrictions [3] of photon contribution relate to energy $E \lesssim 10^{20}\text{eV}$.

Some factors can allow to suppress the expected flux of high energy photons. For example, this flux will be essentially suppressed if the photon free – path within the Galaxy is $\sim 10\text{kpc}$ or less. This means, however, that the radio background within the Galaxy must be more then that adopted in [23] for the intergalactic space by a factor of $\sim 100$ or more.

Other important factor is the distribution of the SHDM particles within the halo of Galaxy. Thus, if the SHDM particles compose only relatively small fraction of the mean DM density of the universe then their possible segregation within halos also suppresses the isotropic flux of both galactic protons and photons. But such segregation increases the expected anisotropy of UHECRs with an essential excess of events from the centrum of Galaxy. Other versions of the improved Top – Down models can be related to possible variations of composition of decay products and processes of proton creation at $E \gg E_{\text{GZK}}$.

If sources of high energy protons are associated with observed galaxies as was recently discussed by Blanton, Blasi and Olinto ([22]) for spectra of injected protons $S(E) \propto E^{-2}$ then restrictions related to the contribution of galactic components of high energy protons and photons become less important but more strong anisotropy of UHECRs is expected. It can be also expected that for such models with $S(E) \propto E^{-0.5}$ or log–normal spectrum of injected protons the resulting flux of UHECRs will be also similar to observed one.

Available observational data do not yet allow to discriminate various explanations of creation of UHECRs with $E \geq E_{\text{GZK}}$ but further observations can give valuable information about particle interactions at ultra – high energy, properties and spatial distribution of SHDM particles and some characteristics of the Galaxy and the universe at both small and high redshifts.

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