

Fluctuations of the superconducting order parameter as an origin of the Nernst effect

K. Michaeli\textsuperscript{1(a)} and A. M. Finkel’stein\textsuperscript{1,2}

\textsuperscript{1} Department of Condensed Matter Physics, The Weizmann Institute of Science - Rehovot 76100, Israel
\textsuperscript{2} Department of Physics, Texas A\&M University - College Station, TX 77843-4242, USA

received 16 January 2009; accepted 31 March 2009
published online 6 May 2009

PACS 72.10.Bg – General formulation of transport theory
PACS 73.50.Lw – Thermoelectric effects
PACS 74.40.+k – Fluctuations (noise, chaos, nonequilibrium superconductivity, localization, etc.)

Abstract – We show that the strong Nernst signal observed recently in amorphous superconducting films far above the critical temperature is caused by the fluctuations of the superconducting order parameter. We demonstrate a striking agreement between our theoretical calculations and the experimental data at various temperatures and magnetic fields. Besides, the Nernst effect is interesting not only in the context of superconductivity. We discuss some subtle issues in the theoretical study of thermal phenomena that we have encountered while calculating the Nernst coefficient. In particular, we explain how the Nernst theorem (the third law of thermodynamics) imposes a strict constraint on the magnitude of the Nernst effect.

Copyright © EPLA, 2009

The recent observations of a transverse thermoelectric signal in the presence of a magnetic field (the Nernst effect) well above the critical temperature of the superconducting transition ($T_c$) both in conventional and in high-$T_c$ material have made this phenomenon an area of high theoretical interest [1,2]. The Nernst effect in high-$T_c$ superconductors [3,4] has been attributed to the motion of vortices [5–7] existing even above $T_c$ (the vortex-liquid regime). In conventional amorphous superconducting films the strong Nernst signal observed deep in the normal state [8,9] cannot be explained by the vortex-like fluctuations. Rather, the authors of refs. [8,9] suggested that the effect is caused by fluctuations of the superconducting order parameter. In this letter, we analyze this mechanism and demonstrate a quantitative agreement between the theoretical expressions and the experiment [9]. No fitting parameters have been used; the values of $T_c$ and the diffusion coefficient have been taken from independent measurements (see refs. [8,9]). In particular, we succeeded in reproducing the non-trivial dependence of the signal on the magnetic field. Our results imply that in the quest for understanding the thermoelectric phenomena in high-$T_c$ materials the fluctuations of the order parameter should also not be ignored.

In metallic conductors, the quasi-particle excitations yield a negligible contribution to the Nernst effect and to its counterpart, the Ettingshausen effect. Under the approximation of a constant density of states at the Fermi energy, which is a standard approximation for the Fermi liquid theory, this contribution vanishes completely [10]. On the other hand, there is no general reason why the collective modes describing all kinds of fluctuations should not contribute to the Nernst effect (in our opinion, the opposite statement in ref. [11] has not been justified). Obviously, neutral modes are not deflected by the Lorentz force and cannot contribute to the transverse-voltage signal. However, the charged modes, such as fluctuations of superconducting order parameter, can be a source for the strong Nernst effect even far from the superconducting transition.

The contributions to the electric conductivity caused by the superconducting fluctuations (paraconductivity) have already been known for forty years [12–14]. Close enough to the superconducting transition the paraconductivity increases rapidly and may even overcome the Drude conductivity. Far from the transition, the superconducting fluctuations produce only one among many corrections to the conductivity and, therefore, can hardly be identified. Owing to the fact that in the absence of fluctuations the Nernst effect is negligible, measurements of the Nernst signal provide a unique opportunity to study.

\textsuperscript{(a)}E-mail: karen.michaeli@weizmann.ac.il
the superconducting fluctuations deep inside the normal state.

The transport coefficients for the electric and heat currents are defined via the standard conductivity tensor:

$$
\begin{pmatrix}
J_e \\
J_h
\end{pmatrix} = \begin{pmatrix}
\hat{\sigma} \\
\hat{\alpha}
\end{pmatrix} \begin{pmatrix}
E \\
-\nabla T
\end{pmatrix}.
$$

When the thermo-magnetic phenomena are studied in films (or layered conductors), the magnetic field is conventionally directed perpendicularly to the conducting plane, see fig. 1. Then each element of the conductivity tensor corresponds to a $2 \times 2$ matrix describing the conductivity components in the $(x, y)$-plane (see eq. (1)). The Onsager relations imply that $\sigma_{ij}(H) = \sigma_{ji}(-H)$ and $\alpha_{ij}(H) = T\alpha_{ji}(-H).$ From the condition, $J_e = 0,$ one gets that the Nernst coefficient is

$$
e_N = \frac{E_y}{-\nabla_x T} = \frac{\sigma_{xx}\alpha_{xy} - \sigma_{xy}\alpha_{xx}}{\sigma_{xx}^2 + \sigma_{xy}^2}.
$$

We checked that the second term in the numerator is negligible in comparison to the first one (see the comment below eq. (13)). Therefore, the leading order term for the Nernst coefficient is $e_N \approx \alpha_{xy}/\sigma_{xx}$ and our goal is to find the transverse Peltier coefficient, $\alpha_{xy}.$

In the linear regime, the electric current generated as a response to an external force, such as the electric field, can be found by the Kubo formula [15], which expresses the response in terms of a correlation function. Extending the Kubo formalism to the calculation of the response to the temperature gradient is not trivial because this gradient is not directly connected to any mechanical force. Following the scheme used in the derivation of the Einstein relation, Luttinger [16] made a connection between the responses to the temperature gradient and to an artificial gravitational field. As a result, Luttinger succeeded to relate all transport coefficients with various current-current correlation functions. However, in the presence of interactions, the expression for the heat current becomes a non-trivial function of the interaction. Usually, instead of the full expression for the heat current operator, the operator of a non-interacting electrons is used (see, for example, ref. [17]). Unfortunately, such a simplified version of the Kubo formula has no justification for the problem considered here. In the presence of a magnetic field, the Kubo formalism meets with an additional difficulty when the thermolectric currents are considered. Obraztsov [18] has pointed out that the heat current describing the flow of entropy must also include a contribution from the magnetization [18–20]. Thus, the problem of this approach is that the current cannot be expressed by a correlation function alone.

In the derivation of the thermolectric currents we have decided, instead of applying the Kubo formula, to employ a different approach and to use the quantum kinetic equation [21–23]. One main advantage of this approach as we will show is that the problem of the magnetization current has been automatically solved. In this way, we obtain that the Peltier and Nernst coefficients, which are related to the flow of entropy, vanish as $T \to 0$ in accordance with the third law of thermodynamics [24].

As we will see, the third law of thermodynamics imposes a strict constraint on the structure of the different contributions to the Peltier coefficient.$^1$

**The quantum kinetic approach.** – In the presence of superconducting fluctuations we describe the system using two fields. One is the quasi-particles field $\psi,$ while the other represents the fluctuations of the superconducting order parameter $\Delta.$ The matrix functions $G(r, r', \epsilon)$ and $L(r, r', \omega)$ written in the Keldysh form [21–23] describe the propagation of these two fields, respectively. The propagators depend on the two spatial coordinates because we postpone the averaging over the disorder until the last stage of the calculation. The $\nabla T$-dependent part of the quasi-particles Green function is naturally separated into two terms. The first one describes the readjustment of quasi-particles to the non-uniform temperature when the system is trying to maintain a local equilibrium. In the regime of linear response, this local-equilibrium Green function becomes

$$
\tilde{G}_{loc-eq}(r, r', \epsilon) = \frac{1}{2T} \epsilon \frac{\partial g(r, r', \epsilon)}{\partial \epsilon}.
$$

Here, $g(r, r', \epsilon)$ is the equilibrium quasi-particles Green function at a constant temperature $T.$ We see that the local equilibrium Green function is a straightforward extension of the equilibrium Green function for a non-uniform temperature. Since the same relation holds for the equilibrium and local equilibrium self-energies, $\hat{\sigma}$ and $\hat{\Sigma}_{loc-eq},$ the equation for $\tilde{G}_{loc-eq}$ is a closed equation fully determined by the equilibrium properties of the system.

$^1$Besides the Peltier coefficient, we may independently find the heat current induced by an applied electric field. Thus, the quantum kinetic approach allows us to calculate separately both off-diagonal components of the conductivity tensor (see eq. (1)) and directly verify the Onsager relations.
\[ j_{\text{con}} = -e \nabla v_T \frac{\partial n_F(\epsilon)}{\partial \epsilon} [v_i^R(\epsilon)v_j^R(\epsilon)v_j^A(\epsilon)g^A(\epsilon) + v_i^R(\epsilon)v_j^R(\epsilon)v_j^R(\epsilon)g^A(\epsilon) - v_i^R(\epsilon)v_j^R(\epsilon)v_j^R(\epsilon)g^R(\epsilon)] \\
- g_i^R(\epsilon)v_j^R(\epsilon)v_i^R(\epsilon)v_j^A(\epsilon) - e \nabla v_T \frac{\partial n_F(\epsilon)}{\partial \epsilon} [v_i^R(\epsilon)v_j^R(\epsilon)v_j^R(\epsilon)g^R(\epsilon) - v_i^R(\epsilon)v_j^R(\epsilon)v_j^R(\epsilon)g^R(\epsilon)] \\
- ie \frac{\partial n_F(\epsilon)}{\partial \epsilon} [\Sigma^e_{\nabla_T}(\epsilon) (1 - n_F(\epsilon)) + \Sigma^\omega_{\nabla_T}(\epsilon) n_F(\epsilon)] (g_i^R(\epsilon) - g_i^A(\epsilon)) \\
+ ie \int_{2\pi} \psi_i^R(\omega) L_i^R(\omega) \left[ \Pi^{\omega}_{\nabla_T}(\omega)(1 + n_F(\omega)) - \Pi^{\omega}_{\nabla_T}(\omega)n_F(\omega) \right] (L_i^R(\omega) - L_i^A(\omega)) + \text{c.c.} \quad (9) \]

The other term in the \( \nabla T \)-dependent part of the Green function is

\[ \tilde{G}_{\nabla T}(r, r', \epsilon) = \hat{g}(\epsilon) \tilde{\Sigma}_{\nabla T}(\epsilon) \hat{g}(\epsilon) \]

\[ \frac{i}{2T} \epsilon \left[ \frac{\partial \hat{g}(\epsilon)}{\partial \epsilon} - \hat{v}(\epsilon) \hat{g}(\epsilon) - \hat{g}(\epsilon) \hat{v}(\epsilon) \frac{\partial \hat{g}(\epsilon)}{\partial \epsilon} \right]. \quad (4) \]

The product of matrices should be understood as a convolution in real space. The matrix \( \tilde{v}(r, r', \epsilon) \) is the velocity of the quasi-particles at equilibrium renormalized by the self-energy \( \tilde{\sigma}(r, r', \epsilon) \):

\[ \tilde{v}(r, r', \epsilon) = \frac{-i}{2m} \lim_{r' \to r} \left( \nabla - \frac{ie}{c} A(r) - \nabla' - \frac{ie}{c} A(r') \right) \]

\[ \quad - i(r - r') \tilde{\sigma}(r, r', \epsilon), \]

where \( A(r) \) is the vector potential.

Let us point out an important difference between the two parts of the Green function depending on the temperature gradient, \( \tilde{G}_{\text{loc-eq}} \) and \( \tilde{G}_{\nabla T} \). As has been already mentioned, \( \tilde{G}_{\text{loc-eq}} \) and \( \tilde{\Sigma}_{\text{loc-eq}} \) are a straightforward extension of the equilibrium Green function and self-energy for a non-uniform temperature. On the other hand, the equation for \( \tilde{G}_{\nabla T} \) contains the self-energy \( \tilde{\Sigma}_{\nabla T} \), which by itself is a function of \( \tilde{G}_{\nabla T} \). Thus, this is a self-consistent equation, and in order to find a close expression for \( \tilde{G}_{\nabla T} \), one has to determine the structure of the self-energy.

The equations for the \( \nabla T \)-dependent parts of the superconducting fluctuations propagator remind the first term in eq. (4) for \( \tilde{G}_{\nabla T} \):

\[ \tilde{L}_{\text{loc-eq}}(r, r', \omega) = -\tilde{L}(\omega) \tilde{\Pi}_{\text{loc-eq}}(\omega) \tilde{L}(\omega), \]

\[ \tilde{L}_{\nabla T}(r, r', \omega) = -\tilde{L}(\omega) \tilde{\Pi}_{\nabla T}(\omega) \tilde{L}(\omega). \quad (6) \]

Here, \( \tilde{L} \) is the equilibrium propagator of the fluctuations at temperature \( T \). The self-energy of the superconducting fluctuations \( \tilde{\Pi}(r, r', \omega) \) depends on the temperature gradient through the quasi-particle Green functions. Similar to eq. (5), we define \( \tilde{V}(r, r', \omega) \) to be the “renormalized velocity” of the superconducting fluctuations (with a contact \( s \)-wave interaction):

\[ \tilde{V}(r, r', \omega) = -i(r - r') \tilde{\Pi}(r, r', \omega). \quad (7) \]

Note that in fact \( \tilde{V} \) does not have the dimension of velocity.

For the calculation of the Nernst effect, we need to obtain the expression for the electric current in terms of the \( \nabla T \)-dependent propagators. In the presence of a magnetic field, the electric current is a sum of two terms:

\[ j = j_{\text{con}} + j_{\text{mag}}. \quad (8) \]

The current \( j_{\text{con}} \) can be as usually derived through the continuity equation for the electric charge. Since the field \( \Delta \) carries charge, it is obvious that the charge of the quasi-particles, \( -e|\tilde{\psi}(r)|^2 \), is not conserved unless the charge carried by the superconducting fluctuations is also included. Then, we obtain using the expressions for the \( \nabla T \)-dependent propagators that

Note that the local equilibrium propagators do not contribute to \( j_{\text{con}} \).

Our only assumption in the derivation of eq. (9) is that the current is obtained in the regime of linear response to \( \nabla T \). As we are interested in the Gaussian fluctuations, we expand the expression for the current with respect to the interaction with the superconducting fluctuations. In fig. 2 we give a diagrammatic interpretation for the dominant contributions to the transverse thermoelectric current after averaging over the disorder. The analytical structure and the expression for the vertices of these diagrams have been found from the quantum kinetic equation. In principle, the same diagrams can be calculated using the Kubo formula. However, if for simplicity one uses in the Kubo formula the heat current operator of non-interacting electrons, the resulting expressions for these diagrams differ from those obtained using the quantum kinetic equation. Most important, as one can see from eq. (9), in the quantum kinetic approach the frequency accompanies the renormalized velocity, so that the expression for the electric current is generally of the form \( e\tilde{v}(\epsilon)v_i(\epsilon)g(\epsilon)v_j(\epsilon)\nabla_j T/T \). In other words, the frequency appears together with the velocity that has already been renormalized by the interaction. On the other hand, owing to the fact that the frequency in the simplified version of the Kubo formula is attached to the external vertex before the renormalization of
Fig. 2: The diagrammatic contributions to the thermoelectric current. Diagrams (a) and (b) describe the fluctuation of the superconducting order parameter decorated by three Cooperons and (c) is the Aslamazov-Larkin diagram. (The obvious counterpart diagrams for (a) and (b) are not shown.) These contributions should be supplemented by the magnetization current term.

The velocity, the expression for the current has a totally different structure.

The second contribution to the electric current is from the magnetization current. Since the magnetization current is divergenceless, it cannot be obtained using the continuity equation. Rather, it is found directly from the action:

$$j_{ei}^{mag} = -2ie\nabla \times M(r) \times \lim_{r' \to r} \int \frac{de}{2\pi} \left[ G_{loc-eq}(r'; r, \epsilon) + \hat{G}_\nabla T(r'; r, \epsilon) \right] <, \quad (10)$$

where $M(r)$ denotes the magnetization and the factor of 2 is due to the summation over the spin index. It can be checked that $\hat{G}_\nabla T$ does not contribute to $j_{ei}^{mag}$. On the other hand, the explicit dependence of the local equilibrium Green function on the center of mass coordinate leads to a non-zero contribution to the magnetization current:

$$j_{ei}^{mag} = 2ie\nabla \times M(r) \lim_{r' \to r} \int \frac{de}{2\pi} \left( r + r' \right) \nabla T \frac{\partial \hat{g}^<(r, r', \epsilon)}{\partial \epsilon} \right). \quad (11)$$

Thus, $G_{\nabla T}$ and $G_{loc-eq}$ are complementary to each other; while the first contributes only to $j_{ei}^{con}$, the other one fully determines $j_{ei}^{mag}$. One should recall that we are looking for a current that does not vanish after spatial averaging, i.e., after integration with respect to the center of mass coordinate $r$. Since in the process of averaging over $r$ we may integrate by parts, the magnetization current can be written as

$$j_{ei}^{mag} = 2ie\nabla \times M(r) \lim_{r' \to r} \int \frac{de}{2\pi} \left( r + r' \right) \nabla T \frac{\partial \hat{g}^{<}(r, r', \epsilon)}{\partial \epsilon} \right) \equiv -\tilde{e}_{ij}c(M_z) \frac{\nabla T}{T}, \quad (12)$$

where $\tilde{e}_{ij}$ is the anti-symmetric tensor. In the transition between eqs. (11) and (12), we integrated by parts over the frequency as well. The result demonstrates the strength of the quantum kinetic approach. This method provides a way to derive both components of the current quantum mechanically without engaging any thermodynamical arguments. At this point, we may employ in eq. (12) the known expression for the magnetization in the presence of superconducting fluctuation:

$$j_{ei}^{mag} = \tilde{e}_{ij} \nabla_j T \frac{\partial}{\partial H} \ln \left[ L_N^{-1}(\omega_m) \right], \quad (13)$$

$$L_N^{-1}(\omega_m) = -\nu \left[ \ln \frac{T}{T_c} + \psi \left( \frac{1}{2} + \frac{\omega_m}{\Omega_c(N + 1/2)} \right) \right. \right.$$

$$\left. \left. -\psi \left( \frac{1}{2} \right) + i\omega_m \right]. \right.$$
The line \( \ln(H/H_c(T)) = 4\pi T/\Omega_c \) separates the regions of classical and quantum fluctuations.

For a small magnetic field, \( \Omega_c \ll T \), close to the transition temperature \( T \approx T_c \), the leading contribution to \( \alpha_{xy} \) is given by the Aslamazov-Larkin term (see fig. 2(c)) and the magnetization current:

\[
\alpha_{xy} \approx \frac{e\Omega_c}{192\pi^2 T \ln T/T_c(H)}.
\]  

Note that unlike the electric conductivity, \( \sigma_{xx} \), for which the anomalous Maki-Thompson [13] and the Aslamazov-Larkin terms yield comparable corrections, the contribution from the anomalous Maki-Thompson term to the Nernst signal is \( \sim (T/\varepsilon_F)^2 \ll 1 \) smaller than the one given by eq. (14). Therefore, it is natural that in the vicinity of \( T_c \) our result coincides with the expression [14,26] obtained phenomenologically from the time-dependent Ginzburg-Landau equation (TDGL).

When temperature is increased further away from the critical temperature, the sum of the contributions to the transverse Peltier coefficient from all the diagrams and the magnetization current yields

\[
\alpha_{xy} \approx \frac{e\Omega_c}{24\pi^2 T \ln T/T_c}.
\]  

The comparison of our result with the experimental observation of ref. [9] for a \( \text{Nb}_{0.15}\text{Si}_{0.85} \) film of thickness 35 nm and \( T_c = 380 \text{mK} \) is given in fig. 4. The Peltier coefficient depends on the mean field temperature of the superconducting transition, \( T_{cMF} \), and on the diffusion coefficient through \( \Omega_c \). Throughout the paper we fit the data using the same diffusion coefficient \( D = 0.187 \text{cm}^2/\text{s} \), which is within the measurement accuracy of the value that has been extracted from the experiment in ref. [9]. We take \( T_{cMF} = 385 \text{mK} \), which is slightly higher than the measured critical temperature anticipating a small suppression of the temperature of the transition by fluctuations. (An equally well fitting of the data has been obtained for a thinner film of thickness 12.5 nm.)

In the vicinity of \( T_c \), one can interpret the expression in eq. (14) in terms of the classical picture in which the Cooper pairs with a finite lifetime are responsible for the thermoelectric current. Far from the critical temperature, the quantum nature of the fluctuations reveals itself in contributions to \( j^\text{con} \) and \( j^\text{mag} \) that are of the order \( \ln(1/T\tau) - \ln(T/T_c) \). However, these \( \tau \)-dependent terms in \( j^\text{con} \) and in the magnetization current cancel each other out. Thus, the third law of thermodynamics constrains the magnitude of the Nernst signal not only at \( T \to 0 \) but also at high temperatures, \( T \gg T_c \).

Finally, we present the expressions for the Nernst signal in the high magnetic-field part of the phase diagram, \( \Omega_c \gg T \). As has been discussed above, after the cancelation of the diverging terms, the remaining contributions to \( \alpha_{xy} \) in the limit \( T \to 0 \) are linear in the temperature:

\[
\alpha_{xy} \approx \frac{eT \ln 3}{3\Omega_c (\ln H/H_{c2}(T))^2}, \quad \text{for } H \approx H_{c2}
\]  

and

\[
\alpha_{xy} \approx \frac{2eT}{3\Omega_c \ln H/H_{c2}}, \quad \text{for } H \gg H_{c2}.
\]  

Notice that \( \alpha_{xy} \) changes its sign in this region. Since the transverse signal is non-dissipative the sign of the effect is not fixed. Although we are in the low-temperature limit, as we have already explained, the integrals determining \( \alpha_{xy} \) accumulate at low frequencies. This situation is rather peculiar; it is not typical for fluctuations induced by a quantum phase transition.

In fig. 5, we plot the curve for the Peltier coefficient as a function of the magnetic field at a temperature higher than \( T_c \). Figure 5 demonstrates the agreement between the theoretical expressions and the experimental observation for a broad range of magnetic fields. In addition, we show that the experimental data is well described by eq. (14) in the limit of vanishing magnetic field (see inset of fig. 5). Since eq. (14) is valid in the limit \( \Omega_c \ll T \),
it can describe only the first few points in the measurement. In order to fit the entire range of the magnetic field, we had to include higher-order terms of \( \Omega_c/T \). For that we needed to sum the contributions from all diagrams and the magnetization current. We performed the calculation assuming that \( \ln (T/T_c(H)) \ll 1 \); therefore, the theoretical curve starts to deviate from the measured data when \( \ln (T/T_c(H)) \) is no longer small (\( H \approx 1 \text{ tesla} \)).

**Summary.** – In this letter we have demonstrated that the fluctuations of the superconducting order parameter are responsible for the large Nernst effect observed in disordered films far away from the transition. Under the condition of the experiment [8,9], the signal generated by the fluctuations dominates the one produced by the quasi-particles up to \( T \lesssim 10^{-2} T_c \) and \( H \lesssim 10^{-2} H_{\text{c2}} \). We have outlined the main steps in the derivation of the Nernst effect using the quantum kinetic equation. In this method one gets automatically all contributions to the Nernst coefficient as response to the temperature gradient, in particular the one from the magnetization current. We have shown that the important role of the magnetization current is in canceling the quantum contributions, thus making the Nernst signal compatible with the third law of thermodynamics. The third law of thermodynamics constrains the magnitude of the Nernst signal not only at low temperatures, but also far from \( T_c \). As a consequence of this constraint, the phase diagram is less rich and diverse than one expects in the vicinity of a quantum phase transition.

The Nernst effect provides an excellent opportunity to test the use of the quantum kinetic equation in the description of thermoelectric transport phenomena. We should remark that our results are different in few aspects from the expressions for the Peltier coefficient recently obtained using the Kubo formula in ref. [27]. The striking agreement between our results and the experiment in the different limits (and the fact that we have reproduced the phenomenological result of the TDGL [26]) reinforces us in the correctness of our method.

***

We thank H. Aubin, K. Behnia, J. Sinova, M. A. Skvortsov, and A. A. Varlamov for valuable discussions. The research was supported by the US-Israel BSF and the Minerva Foundation.

REFERENCES

[1] Zaanen J., Nature, 448 (2007) 1000.
[2] Hartnoll S. A., Kovtun P. K., Muller M. and Sachdev S., Phys. Rev. B, 76 (2007) 144502.
[3] Xu Z. A., Ong N. P., Wang Y., Kakeshita T. and Uchida S., Nature, 406 (2000) 486.
[4] Wang Y., Li L. and Ong N. P., Phys. Rev. B, 73 (2006) 024510.
[5] Anderson P. W., Nat. Phys., 3 (2007) 160.
[6] Podolsky D., Raciu S. and Vishwanath A., Phys. Rev. Lett., 99 (2007) 117004.
[7] Mukherjee S. and Huse D. A., Phys. Rev. B, 70 (2004) 014506.
[8] Pourret A. et al., Nat. Phys., 2 (2006) 683.
[9] Pourret A. et al., Phys. Rev. B, 76 (2007) 214504.
[10] Sondeheimer E., Proc. R. Soc. London, Ser. A, 193 (1948) 484.
[11] Sergeev A., Reizer M. Y. and Mitin V., Phys. Rev. B, 77 (2008) 064501.
[12] Aslamazov L. G. and Larkin A. I., Fiz. Tverd. Tela, 10 (1968) 1104 (Sov. Phys. Solid State, 10 (1968) 875).
[13] Maki K., Prog. Theor. Phys., 40 (1968) 193.
[14] Larkin A. I. and Varlamov A. A., Theory of Fluctuations in Superconductors (Clarendon, Oxford) 2005.
[15] Kubo R., J. Phys. Soc. Jpn., 12 (1957) 570.
[16] Luttinger J. M., Phys. Rev., 135 (1964) A1505.
[17] Niven D. R. and Smith R. A., Phys. Rev. B, 71 (2005) 035106.
[18] Obraztsov Y. N., Fiz. Tverd. Tela, 7 (1965) 573 (Sov. Phys. Solid State, 7 (1965) 455).
[19] Smir'ko L. and Streda P., J. Phys. C: Solid State Phys., 10 (1977) 2153.
[20] Cooper N. R., Halperin B. I. and Ruiz I. M., Phys. Rev. B, 55 (1997) 2344.
[21] Keldysh L. V., Zh. Eksp. Teor. Fiz., 47 (1964) 1515 (Sov. Phys. JETP, 20 (1965) 1018).
[22] Rammer J. and Smith H., Rev. Mod. Phys., 58 (1986) 323.
[23] Haug H. and Jauho A.-P., Quantum Kinetics in Transport and Optics of Semiconductors (Springer, Berlin) 1996.
[24] Hu C.-R., Phys. Rev. B, 14 (1976) 4834.
[25] Aronov A. G., Hikami S. and Larkin A. I., Phys. Rev. B, 51 (1995) 3880.
[26] Usishkin I., Sonnhi S. L. and Huse D. A., Phys. Rev. Lett., 89 (2002) 287001.
[27] Serbyn M. N., Skvortsov M. A., Varlamov A. A. and Galitski V., arXiv:0806.4427 preprint (2008).