Breaking one into three: surface-tension-driven droplet breakup in T-junctions

Jiande Zhou,1 Yves-Marie Ducimetière,2 Daniel Migliozzi,1 Ludovic Keiser,2,3 Arnaud Bertsch,1 François Gallaire,2 and Philippe Renaud1

1Laboratory of Microsystems (LMS4), EPFL, CH1015 Lausanne, Switzerland
2Laboratory of Fluid Mechanics and Instabilities, EPFL, CH1015 Lausanne, Switzerland
3Univ. Grenoble Alpes, CNRS, LIPhy, 38000 Grenoble, France

(Dated: July 4, 2022)

Droplet breakup is an important phenomenon in the field of microfluidics to generate daughter droplets. In this work, a novel breakup regime in the widely studied T-junction geometry is reported, where the pinch-off occurs laterally in the two outlet channels, leading to the formation of three daughter droplets, rather than at the center of the junction for conventional T-junctions which leads to two daughter droplets. It is demonstrated that this new mechanism is driven by surface tension, and a design rule for the T-junction geometry is proposed. A model for low values of the capillary number $Ca$ is developed to predict the formation and growth of an underlying carrier fluid pocket that accounts for this lateral breakup mechanism. At higher values of $Ca$, the conventional regime of central breakup becomes dominant again. The competition between the new and the conventional regime is explored. Altogether, this novel droplet formation method at T-junction provides the functionality of alternating droplet size and composition, which can be important for the design of new microfluidic tools.

I. INTRODUCTION

Droplet formation is a ubiquitous process in both nature and industry. In the context of microfluidics, the controllable generation of micro-droplets has enabled a wide range of applications, opening a new era for biological and chemical analysis and synthesis [1-3]. The formation of droplets is the first step to achieve in the pipeline in order to achieve versatile functionalities such as microreactors [4,5], mini-incubators [6,8], material templates [9,11], digital counters [12,14], or single cell platforms [15-18]. To date, droplet formation mechanisms in rectangular microchannels have been widely studied and can be classified in two main categories [19-24]: the mechanisms driven by hydrodynamic forces and those driven by surface tension. In the former category, the carrier flow is brought to the dispersed phase to generate viscous and/or inertial forces destabilizing the interface, and surface tension acts as the stabilizing force. In the latter, the interface breakup is purely driven by an imbalance in capillary pressure induced by an abrupt change of confinement [25]. The first category of droplet production processes is flexible in operation and advantageous in producing a high droplet throughput [6,22,24]. Although limited by the flow rate, the second category is advantageous for monodisperse droplet production and parallelization [27,29].

Droplet formation can result from the emulsification of a continuous phase, or from the breakup of an existing droplet. The latter process enables to adjust the initial droplet size, to increase droplet production rate or to provide new functionalities, such as up-concentration [30,31]. One of the most studied geometry for droplet breakup is the T-junction, where a straight channel splits perpendicularly into two lateral channels. Following the seminal work by Link, et al. [32], various studies have investigated the dynamics of the droplet breakup process, for both short [33-39] and elongated droplets [40-46]. Other studies also investigated how to modify the topology of the T-junction to perform asymmetric droplet breakup [47,49]. In all those configurations, droplets don’t breakup at small capillary numbers $Ca = \frac{\mu V}{\gamma}$, and are split into two daughter droplets above a critical capillary number $Ca_c = \frac{\mu V}{\gamma}$, with $\mu$ the viscosity of the carried fluid, $\gamma$ the interfacial tension and $V$ the speed of the droplet. The breakup process is here driven by the hydrodynamics stress exerted by the carrier flow which enables to deform and break the interface.

In this study, we report a novel droplet break-up regime in T-junctions that is surface-tension-driven. In this regime, the droplet interface ruptures symmetrically in the two lateral channels away from the junction, which gives birth to three daughter droplets instead of two. We show that this regime only occurs in T-junctions that have a different aspect and width ratio compared to the ones presented so far in the scientific literature until now. The height $h$ of the channels must be larger than the width of the inlet channel $w_i$, which itself must be larger than the width of the outlet channel $w_o$: $h > w_i > w_o$. We describe the underlying mechanism of the new droplet breakup mechanism and provide a geometry design rule predicting the occurrence of the new regime in a T-junction. We also propose a semi-quantitative model accounting for the gutter flows to describe the dynamical process of the new breakup regime. Finally, we show that the conventional central breakup also occurs in the new T-junctions under certain flow conditions. Both central and lateral breakup regimes can develop independently, but the droplet breakup regime actually occurring is the faster one.
FIG. 1. (a) Geometry of the T-junctions used throughout our study: both aspect ratio $h/w_o$ and width ratio $w_i/w_o$ are larger than unity. The eye shows the observation perspective during experiment. (b) Time sequence of a lateral breakup process for a short (blue) and a long (red) droplet. Inset shows the interface at the moment of rupture (red arrow), captured at a frame rate of 50,000 fps.

II. EXPERIMENTAL AND NUMERICAL METHODS

A. Device fabrication

To create the microchannels, a silicon mold fabricated by Dry Reactive Ion Etching (DRIE) was used. First, a 1.5 $\mu$m photoresist layer was deposited on double side polished silicon wafers, and was patterned with standard photolithography including steps of exposure and development to obtain the 2D channel shape. The exposed wafer area was then etched using the Bosch process (DRIE, Alcatel AMS 200). The obtained channel depth is proportional to the etching duration, and the value is measured with a surface profilometer (Tencor Alpha-Step 500). After the Si mold was silanized within a trichlor-(1H,1H,2H,2H-perfluorocetyl) (PFOTs)-filled desiccator for five hours, we pour PDMS pre-polymer (1:10 ratio mixture) onto the Si mold and cure in 80°C oven for three hours. We peel the PDMS replicas from the mold and after punching inlet and outlet holes seal the channels by bonding to a PDMS-coated glass slide (oxygen plasma bonding, 500 mTorr, 45 sec, 29 W). Coating of the glass slide (standard 25mm * 75mm * 1mm) is done by spin coating a thin layer of PDMS pre-polymer at 1700 rpm for 35s, then cure in the oven (as above). The hydrophobicity of the surfaces was naturally regained by placing PDMS in the oven for 3 days.

B. Experiments

The experiments were performed under an inverted microscope (Nikon Eclipse TE 300) and imaged with a high-speed camera (Phantom Miro M310). Syringe pump (CETONI Nemesys) with gastight glass syringes (Hamilton) is used to control the flowrates injected into the system. Depending on the flow rates, frame rates up to 50,000 frames per second were used for recording the droplet breakup process. A customized ImageJ script is used to automatically recognize the droplets and obtain the intensity profile. A MATLAB (Mathworks) script is used for calculating the droplet speed and length. The results were confronted to the observations to ensure accuracy.

C. Numerical simulations

The closed system for the three unknowns $\bar{z}(\eta,t)$, $\bar{k}(\eta,t)$ and $L_p(t)$ from equations (14) and (16) was solved numerically using the COMSOL Multiphysics software, based on the finite element method. More precisely, the system (14) is implemented directly in the "General form PDE" component of the software, and its weak form has been spatially discretized over the interval $\xi \in [0,1]$ using first-order polynomials (corresponding to a linear interpolation of the solution). The convergence of the numerical results with respect to the spatial discretization has been verified. Equation (16), enforcing the volume conservation thus depending only on time, is implemented in the "Global Equations" component. The system is marched in time using the backward differentiation formula ("BDF"), and the results are sought for 4000 discrete times uniformly distributed between 0 and $10/Ca$. A stopping condition has been added, such that the simulation stops running if $\min(\bar{z}) < 1/2$. Concerning the nonlinear, fully coupled solver, the default
III. RESULTS

A. Description of a novel breakup mechanism

In previous studies, droplet breakup was conducted in T-junctions, where the inlet and outlet channels have the same width and where the channel height is equal to or smaller than the width \cite{32,33,14}. In this study, we use a non-conventional T-junction (Figure 1a) with the inlet and outlet width \((w_i\) and \(w_o\) respectively) and the height of the channel \((h)\) fulfilling \(h > w_i > w_o\). Consequently, both the aspect ratio \((h/w_o)\) and the width ratio \((w_i/w_o)\) are larger than unity. Upstream of the T-junction, water-in-oil droplets are generated using a flow-focusing device with two inlets, one introducing deionized water (dispersed phase) and the other fluorinated oil (continuous phase). A third inlet introduces additional oil downstream of the flow-focusing unit in order to separate the droplets and further control their speed. When a droplet passes through the T-junction and fully enters the lateral channels, its rear interface remains pinned at the junction with a constant and convex curvature, whereas the front interfaces advance further downstream. This is in contrast with the central breakup mechanism which features a progressive concave curving of the rear interface during breakup \cite{32}. Eventually, it is the interfaces inside the lateral channels that collapse and create two new interfaces at a symmetric distance from the junction. This type of breakup creates three daughter droplets rather than two (which is observed during the classical breakup at T-junction). This breakup is referred to as lateral breakup, in comparison to the classical central breakup described in the literature. Two examples of droplets undergoing a lateral breakup are presented in Figure 1b. The collapse is very rapid but can be captured by a high speed camera (inset).

The interface appears to break very suddenly during the time the rear cap remains pinned at the junction. It suggests that the necking process, which is usually more gradual, is likely acting off-plane before the final pinch-off happens.

B. Geometric conditions required for the lateral breakup

We first detail the geometry of the T-junction which enables the lateral breakup phenomenon. Using a quasi-static assumption, we consider that the Young-Laplace equation controls the pressure drop across the interface of the droplet: \(p_d - p = \gamma \kappa\), where \(p_d\) is the pressure in the drop, \(p\) is the pressure in the surrounding fluid at the interface (Figure 2a), \(\gamma\) is the interfacial tension, and \(\kappa\) is the local mean curvature of the interface. When the droplet passes through a T-junction whose outlet channels have smaller dimension than the inlet channel \((w_o < w_i)\), the curvature at the front of the droplet \(\kappa_o\) increases compared to the curvature at the rear \(\kappa_i\), thereby creating a pressure gradient along the droplet interface. We assume that the dominant pressure variations occur in the gutters present in the corners of the cross-section, and consider that the pressure in the droplet \(p_d\) can be roughly considered as constant in space and time \cite{32,33}. It implies that in the fluid surrounding the droplet, the pressure gradually decreases from the rear cap in the inlet channel \((p_i = p_d - \gamma \kappa_i)\) to the front cap in the outlet channels \((p_o = p_d - \gamma \kappa_o)\), by continuity. This pressure gradient is accompanied by an adaptation of the radius of the gutter \(R_g\), such that \(p = p_d - \gamma / R_g\). Along the droplet, \(R_g\) thus varies from \(1/\kappa_i\) in the rear of the droplet to \(1/\kappa_o\) in the front. In the quasi-static condition, the value of \(\kappa_i\) and \(\kappa_o\) is constant and only dependent on the channel geometry\cite{51}:

\[
\kappa_{i,o} = \frac{1 + \frac{w_{i,o}}{h}}{\frac{w_{i,o}}{h} + \sqrt{\left(1 - \frac{w_{i,o}}{h}\right)^2 + \frac{\pi \frac{w_{i,o}}{h}}{h}}}
\]

where \(i\) and \(o\) respectively account for inlet and outlet. However due to the confinement and the non-wetting condition, \(R_g\) cannot exceed a threshold value given by half of the smallest dimension of the cross-section \cite{27}. In our case \(w_o < h\) which gives a critical value \(R_g^*=w_o/2\). Consequently, if the relatively large pressure imposed in the gutter by the proximity of the rear cap imposes a radius of curvature \(R_g^*\) larger than \(R_g^*\) in the outlet channels, an instability is triggered (Figure 2b). In order to fulfill the continuity of pressure along the channel, the interface has to curve concavely in the \(y\) direction, which marks the initiation of a necking process. A “pocket” thus gradually inflates at the upper and bottom part of the channel between the droplet and the \((x,y)\)-walls, where the continuous phase accumulates. The droplet thereby thins down (necking process) until reaching a quasi-cylindrical shape, when surface tension induces a final and sudden breakup. Such a necking process is off-plane until the last
FIG. 2. Capillary instability responsible for lateral breakup (a) Presentation of key droplet parameters with a top view of a T-junction through which a droplet splits. (b) Cross sectional view in the outlet channel (indicated by black arrowheads in (a)) showing three different gutter radius. These three conditions can hold for the same droplet passing the junction at different times. When $R_g > R^*_g$, the necking starts. (c) Colormap representing $\beta$ in a diagram representing the aspect ratio $h/w_o$ as a function of the width ratio $w_i/w_o$. Blue region corresponds to $\beta < 1$, i.e. geometries that do not allow the occurrence of lateral break-up; Green regions correspond to $\beta > 1$, i.e. geometries prone to exhibit lateral breakup. Each marker corresponds to one of the geometries experimentally tested (see Table I). A black symbol correspond to an absence of lateral breakup observed, and a red marker corresponds to a presence of a lateral breakup.

moment of rupture, which is in consistence with the experimental observation. The lateral breakup most often occurs simultaneously in both outlet channels.

| Geometry | $w_i$ [µm] | $w_o$ [µm] | $h$ [µm] | $h/w_o$ | $w_i/w_o$ | $k_i$ | $\beta$ | Ca range | Lateral breakup |
|----------|-------------|-------------|-----------|---------|-------------|------|--------|----------|----------------|
| A        | 30          | 14          | 62        | 4.2     | 2.1         | 0.09 | 1.5    | 0.005-0.30 | Yes            |
| B        | 30          | 14          | 37        | 2.6     | 2.1         | 0.11 | 1.2    | 0.006-0.077 | Yes            |
| C        | 30          | 14          | 5         | 0.4     | 2.1         | 0.45 | 0.3    | 0.006-0.107 | No             |
| D        | 60          | 14          | 37        | 2.6     | 4.3         | 0.08 | 1.7    | 0.004-0.183 | Yes            |
| E        | 45          | 14          | 37        | 2.6     | 3.2         | 0.09 | 1.5    | 0.014-0.138 | Yes            |
| F        | 30          | 30          | 80        | 2.8     | 1           | 0.09 | 0.8    | 0.006-0.160 | No             |
| G        | 100         | 12          | 37        | 3.1     | 8.3         | 0.07 | 2.4    | 0.035-0.73  | Yes            |
| H        | 30          | 12          | 85        | 7.1     | 2.5         | 0.09 | 1.9    | 0.02-0.04   | Yes            |

Note that the necking criterion $R_g > R^*_g = w_o/2$ is analogous to the one ruling step emulsification [25] or snap-off processes. The geometric criterion for a T-junction to allow a passing droplet meet the necking condition of $R_g > R^*_g$ can be expressed as $1/\kappa_i > R^*_g$. Defining the confinement parameter $\beta$ as $\beta = 2/(\kappa_i w_o)$, the lateral breakup will thus be prone to happen when $\beta > 1$, i.e. when:

$$\beta = \frac{2}{1 + \frac{w_i}{\kappa_i} + \sqrt{\left(1 - \frac{w_i}{\kappa_i}\right)^2 + \pi \frac{w_i}{\kappa_i}}} > 1.$$  (2)

To test the criterion of Eq.2 we select eight T-junction geometries with different combinations of $h/w_o$ and $w_i/w_o$ on which droplet breakup experiments are conducted with varying Ca (see Table I). The outcomes of those experiments
are represented in Figure 2c). No lateral breakup was observed for the two geometries with $\beta < 1$, while geometries that have $\beta > 1$ always showed lateral breakup for a given range of $Ca$ and $L$. In addition, with extreme $\beta$ value the lateral breakup phenomenon is significantly enhanced (more details in Appendix). Both observations confirm $\beta$ as a good proxy to evaluate the 'proneness' of the lateral breakup. We rearrange equation (2) and map in fig 2c(ii) the $\beta$ value of a geometry as a function of its width ratio $w_i/w_o$ and aspect ratio $h_i/w_o$, where the green to yellow region represents the geometrical conditions of $\beta > 1$, which should allow the lateral breakup to occur. Note that a higher $\beta$ value is always associated with a larger aspect ratio and/or a larger width ratio, shown in the contour map as markers that are further and further away from the diagonal. It suggests that the capillary instability leading to the lateral breakup is driven by both of the two ratios. Indeed, the high aspect ratio ($h > w_o, h > w_i$) ensures that the confinement level on a droplet is dictated by the channel width (the smaller dimension). Then, the large width ratio ($w_i > w_o$) actually imposes the difference of confinement on the same droplet crossing the junction. Both conditions together create the necessary capillary pressure imbalance that eventually drives the lateral breakup.

C. Modelling the dynamics of the lateral breakup for lower $Ca$

Next, we derive a theoretical model to describe the dynamics of the lateral breakup, occurring in two steps: 1. The droplet progresses through the channel until the necking criterion is met- this is the onset of the necking; and 2. The necking-induced pocket of continuous phase, fed via the gutters, inflates and thins down the droplet until final pinch-off. The first step is to find the condition where a minimal value of $1/R_g^* = 2/w_o$ is met within the outlet channel. At an initial configuration, a droplet of speed $Ca$ and an initial length $L(0)$ (not shown) passes the junction, creating gutters of length $L_i$ and $L_o$ in the inlet and outlet channel. We assume a homogeneous pressure $p_d$ inside the droplet, and obtain a hydraulic resistance per unit length:

$$r_h(s,t) = \frac{C\mu}{(1-\pi/4)R_g(s,t)^2},$$

(3)

where $\mu$ is the viscosity of the fluid, $C$ is a geometric constant with $C = 93.93$ [52], and $R_g(s,t)$ is the radius of the gutter along the droplet internal coordinate $s$. Note that $s$ is oriented along $x$ in the inlet channel and along $y$ in the right outlet channel. At the rear and front caps we have $R_g(0,t) = R_i$ and $R_g(L(t),t) = R_o$, where $R_i,o = \kappa_{i,o}^{-1}$ is the inverse of the total curvatures of the caps defined in eq. (1). The difference between the two induces a flow rate $q(t)$ of the continuous phase, allocated in 4 gutters in the inlet channel and in 2 $\times$ 2 gutters in the outlet channels. Experimentally, we observed a reduction of droplet rear cap speed after the front cap enters the outlet channel (Figure 3b), which confirms the presence of this total bypass flux $q(t)$. Combining the Young-Laplace equation for the pressure balance at the interface $p(s,t) = p_d - \gamma/R_g(s,t)$ and the Poiseuille equation expressing the pressure gradient within the continuous phase $\partial p/\partial s = -r_h q/4$, one obtains an equation controlling the shape of the gutters:

$$\frac{\partial R_g^3(s,t)}{\partial s} = -\frac{q(t)}{4\gamma} \frac{C\mu}{(1-\pi/4)R_g(s,t)^2},$$

(4)

with a continuous change of gutter radius $R_g^3(s,t)$ along the droplet from $F_i$ to $F_o$. The quantity $L(t) = L_i(t) + L_o(t)$ designates the total length of the droplet (excluding caps) along $s$ the internal abscissa, and is determined by volume conservation from known initial droplet length $L(0)$ and $L_i(t)$ (see Appendix). Solving equation (4) provides both $q(t)$ -constant in space due to flow rate conservation- and the gutter radius $R_g^3(s,t)$ at any location ($s$) along the droplet:

$$q(t) = \frac{(F_i^3 - F_o^3)}{AL(t)},$$

(5)

$$R_g^3(s,t) = F_i^3 - q(t)As \quad \text{for} \quad 0 \leq s \leq L(t),$$

(6)

where $A = 3C\mu/(4\gamma(1-\pi/4))$. By progressively decreasing $L_i$ from $L(0)$ (the droplet turns the junction at $t=0$), we find the critical $L_{ic}$ such that $R_g = R_g^* = w_o/2$. Further advancing the droplet, $R_g > w_o/2$ cannot be met, and the necking has to start. The corresponding critical time $t_c$ can be obtained from $L_{ic} = L(0) - Ca t_c$. Figure 3c plots $R_g^3$, changing linearly from $F_i^3$ to $F_o^3$ along the droplet, for three time-stamps and corresponding droplet locations during the advancing of the droplet. It illustrates the following scenario for the onset of the necking: with the droplet advancing in the channel, the rear cap approaches the junction and increases more and more the gutter radius in the outlet channel, which eventually goes beyond the maximum possible value fixed by the outlet channel geometry, thus falling out of balance. Such process is strongly influenced by the flow rate and droplet size which change the slope.
The colormap represents the normalized local pocket depth $z_L$ of the pocket predicted by the model (for geometry $w_o/h = 14/62$, $w_i/h = 30/62$, with initial droplet length of $L/w_o = 8$ and capillary number of $Ca = 0.005$). The vertical axis corresponds to the $\eta$ coordinate (non-dimensionalized with $w_i$), and the length of $L_p(t)$ and $L_o(t)$ are drawn in color and grey respectively as a function of non-dimensional time (horizontal axis); The colormap represents the normalized local pocket depth $z(s,t)/h$ with the simulation stopped when $z(s,t)/h$ goes below $(w_o/h)/2 \approx 0.11$.

and length of the $R_g$ curve. As the maximum gutter radius along the outlet channel is always attained at the junction location $(s_J)$, it is always at the junction that the necking requirement is first met. Thus, the pocket of continuous phase is expected to start forming from the junction, which is confirmed by the experiment, as discussed below.

Now, the droplet enters a second phase consisting in the development of the pocket. To model the evolution of such process, we divide the droplet into three consecutive parts (Figure 3a): the part in the inlet channel of length $L_i(t)$ with gutters; The part on the spatial interval of $0 \leq \eta \leq L_p$, where $L_p(t)$ is the length of the pocket, from the junction ($\eta = 0$) to where the droplet curvature in the direction of the flow vanishes ($\eta = L_p(t)$). The third part corresponds to the remaining of the droplet in the outlet channels where the gutter is resumed, of length $L_o(t)$. In the pocket region, we parametrize the droplet surface by its curvature in the flow direction (i.e, the curvature in the
y − z plane in Figure 3a), defined as

\[ k(\eta, t) = -\frac{\partial}{\partial \eta} \left[ \frac{\partial z(\eta, t)/\partial \eta}{\sqrt{1 + (\partial z(\eta, t)/\partial \eta)^2}} \right]. \]  

(7)

Where \( z \in [w_o/2; h/2] \) designates the interfacial position: \( z \) equals to \( h/2 \) when no pocket is formed and gutters are maintained, and \( z = w_o/2 \) corresponds to a cylindrical droplet cross section that represents the end point of the pocket development. The curvature in the direction perpendicular to the flow, i.e., the curvature in the x − z plane in Figure 3a, is assumed constant and equals to \( 2/w_o \), such that the total curvature of the droplet in the pocket region writes \( k(\eta, t) + 2/w_o \). We then define the continuity equation for the continuous phase as \( \partial S/\partial t = (\partial q/\partial z)/2 \), where \( S[z(\eta, t)] = (\pi - 4)w_o^2/4 + 2z(\eta, t)w_o \) is the cross-sectional area of the discrete phase in one outlet channel, which is fed by two quarter-sections at the top wall with a flow rate of \( q(\eta, t)/4 \) in each. We apply the derivative to the equation of the pressure balance at the interface to obtain the flow rate

\[ q(\eta, t) = \frac{\gamma}{r_{h,S}[z(\eta, t)]} \frac{\partial k(\eta, t)}{\partial \eta}. \]  

(8)

where \( r_{h,S}[z(\eta, t)] \) designates the hydrodynamic resistance per unit length of a quarter-section, which reduces to equation (3) for \( z = h/2 \). Injecting both the expression for \( S[z(\eta, t)] \) and equation (8) in the continuity equation leads to

\[ \frac{\partial z(\eta, t)}{\partial t} = \frac{4\gamma}{w_o \eta} \frac{\partial}{\partial \eta} \left( \frac{1}{r_{h,S}[z(\eta, t)]} \frac{\partial k(\eta, t)}{\partial \eta} \right), \]  

(9)

such that equation (7) and equation (9) constitute a system of two coupled equations for the two unknowns \( z(\eta, t) \) and \( k(\eta, t) \). It is subject to two boundary conditions for \( z \): \( z(0, t) = z(L_p(t), t) = h/2 \), as well as two for \( k \) : \( k(0, t) = k_J - 2/w_o \), and \( k(L_p(t), t) = 0 \), where \( k_J \) is the curvature of the inlet gutter at the junction, found by matching with the inlet gutter regime (see Appendix). As mentioned, the necking condition has already been met, thus \( k(0, t) \leq 0 \), resulting in the opening of the pocket; however, \( k(\eta, t) \) must increase with \( \eta \) until recovering \( k(L_p(t), t) = 0 \), as the hydrodynamic resistance induces a pressure drop of the continuous phase (see equation (8)). We used a finite element method to calculate the dynamics of the necking process numerically, i.e., \( z(\eta, t) \) and \( k(\eta, t) \). The boundary conditions, numerical discretization and nondimensionalization used for this purpose are detailed in the appendix and numerical methods section. The result of the simulation resolves the pocket evolution process, which can be represented by the change of pocket length \( L_p(t) \) and depth \( z(\eta, t) \) (Figure 3d). It shows that these two quantities increase over time, with a monotonic downstream extension of the pocket boundary. As \( z(\eta, t) = w_o/2 \), a locally cylindrical cross-section is reached during the pocket evolution, which triggers a fast breakup controlled by surface tension.

![Breakup moment of six breakup events with increasing Ca](Image)

FIG. 4. Breakup moment of six breakup events with increasing Ca. The Ca value from top to bottom is 0.016, 0.025, 0.056, 0.088, 0.129 and 0.177. The breakup location in the right outlet channel is shown with black arrowheads. The scale bar represents 30 µm.

This model is restricted to low Ca for two main reasons. First, large values of Ca may lead to a cross-section occupancy of both liquids which is not accounted for in our gutter model, as evidenced by Lozar et al. [53]. Second, the internal viscous dissipation has an increasing contribution at higher Ca, and was not included in the model.
FIG. 5. (a) Time sequences of example breakup events for the same droplet length under three flow conditions. The breakup regime shifts from lateral to central breakup from low to high Ca. The scale bar represents 30 µm. (b) Kymograph of light intensity along the central part of the outlet channel (white dashed line), for two droplets of the same size but with different regimes; The grey value is turned into colors in the colormap. At time zero, both droplets enter the junction, the trajectory of the front interface forms a straight line. After the rear interface arrives at the junction (inset), the change of intensity due to the light scattering from the interface of the pocket is captured (white arrowheads), which always starts from the junction as predicted. At the end of each process, new interface(s) is formed at the locations indicated by the black arrows. (c) The breakup transition regime map of Ca₀ versus Lo for geometry A (Figure 2c), where Ca₀ = Ca(w_i/wo)/2 and Lo = L(0)w_i/wo/2. Blue and red circles represent lateral and central breakups respectively. The area of each circle is proportional to the characteristic breakup time, defined from when droplet rear interface reaches the junction to the final breakup moment. The black curve represents the function Ca₀ = bLo⁻¹, where b = 1.9 in this case (geometry A). Inset: d_p, the pinch off lateral distance from the junction center (in um) versus the product of Ca₀Lo. (d) Logarithmic representation of the breakup transition regime map for Ca₀ vs. Lo for four geometries (A, B, D, E) with different β values, represented by four colors. The filled and hollow markers represent lateral (LB) and central breakups (CB) respectively. Dashed lines of slope −1 are represented to guide the eyes.

Experimentally, we observed an evolution of lateral breakup behaviour from low to high Ca condition. For lower Ca, a pocket forming process starts and stops before the rear interface reaches the junction. The corresponding breakup distance from the junction decreases with increasing Ca (Figure 4). For higher Ca, the breakup location is stabilized, and an decreasing rear cap curvature is observed as Ca increases (Figure 4). We next discuss the latter case concerning higher Ca.

D. A central breakup recovered at higher Ca

At higher Ca, when a critical Ca* is exceeded, the conventional central breakup regime can be recovered, even for geometries enabling lateral breakup. Figure 5a shows three breakup events with the same droplet size. Central breakup is observed at higher values of Ca, while both lateral and central breakups can occur simultaneously near the critical value Ca*. In Figure 5b, we show light intensity kymographs of two breakup events with the same droplet size but different breakup regimes. The existence of the lateral pocket cannot be imaged directly but it can
be detected by a faint intensity change, caused by the light scattering at the openings. First, it confirms that the necking starts from the junction as predicted by our model (Figure 3). Second, it is remarkable to find out that the pocket formation occurs regardless of the final breakup outcome. This observation, together with the coexistence of lateral and central breakups near the critical \( Ca^* \) indicates that the two processes are simultaneous. It gives a hint on the breakup transition mechanism, attributed to the faster completion of central breakup that aborts the lateral breakup process with the interfacial rearrangement.

We obtained the regime map near the transition zone for \( Ca_o \) versus \( L_o \) in Figure 5c. Here, \( Ca_o = Ca(w_i/w_o)/2 \) is the outlet channel capillary number, and \( L_o = L(0)(w_i/w_o)/w_o/2 \) is the initial droplet length translated into outlet channel (divided by 2 for only one branch) normalized by the outlet width. We compare the characteristic breakup time for both regimes, defined as the duration from the rear cap reaching the corner until the breakup and represented in Figure 5c) as the surface area of the round markers. Interestingly, the characteristic time decreases approximately with increasing \( Ca \) for both regimes. But at each transition point the central breakup always has a shorter characteristic time than the adjacent lateral breakup. From the regime map, a longer droplet needs a lower \( Ca \) for the transition to central breakup. We found that the relation between \( L_o \) and its transition \( Ca^*_o \) can be well described by the scaling law \( Ca^*_o \sim bL_o^{-1} \). The latter is also found to describe the non-breakup/central breakup transition on conventional T-junctions for long droplets [44]. This indicates that the lateral/central breakup transition is probably dictated by the enabling of the central breakup that is the faster process. This leads to a critical constant \( (Ca_oL_o)^* \) that solely governs the lateral/central breakup transition. In the inset of Figure 5c, the separation of the two regimes by \( (Ca_oL_o)^* \approx 1.9 \)

However, this experimentally determined prefactor is much higher than the theoretical value obtained for the same geometry (A) but assuming no lateral breakup following the scaling analysis of Haringa et al. [44] (see Appendix). We note the difference of enabling central breakup on these new T-junctions. The continuous flow arriving at the junction can: (a) bypass the entire droplet through gutters, (b) flows into the lateral pocket and increase its volume, or (c) push the rear cap and contribute to central breakup. In conventional T-junctions, there is no pathway (b), and (a) is negligible at higher \( Ca \). In the lateral breakup-enabled T-junctions, the pathway (a) may be enhanced by an enlarged “gutter” area of the continuous phase when \( Ca \) is high (prominent for high aspect ratio channel [33]). Together with the uniquely presented pathway (b), it indicates that the lateral breakup-enabled T-junction uses a smaller portion of the incoming flow for central breakup compared to a conventional T-junction. This means for the same droplet length \( L_o \), a higher \( Ca^*_o \) is required to enable the central breakup and the transition, reflected by the increased constant \( (Ca_oL_o)^* \). In Figure 5 we maps the breakup regimes near the transition zone for four geometries with the same outlet widths in a logarithmic scale (From geometries A,B,D and E described in the Table). The decay rate of \( Ca^*_o \) with \( L_o \) is similar for all the tested geometries, as a power law with an exponent close to -1, similar to the above observation. The intersect of these -1 laws, proportional to the constant \( (Ca_oL_o)^* \), varies among the geometries. Geometries with more prominent lateral breakup (higher value of \( \beta \)) require a higher \( Ca^*_o \) to recover central breakup.

We also mention that the geometry may alter the relative time scale of the two processes. For example, on geometries that favor less the lateral breakup (e.g. geometry B), there is no lateral/central simultaneous breakup near the transition region, as shown in Figure 5a for geometry A, indicating a much slower lateral breakup at this moment than the central breakup. We thus warn that it is not impossible to have a lateral breakup process terminating before the central breakup process (of droplet flattening, concaving and finally pinching off), provided that a geometry promotes the former to have its process finished earlier. In a nutshell, the droplet breakup fate in these novel T-junctions can: (a) bypass the entire droplet through gutters, (b) flows into the lateral pocket and increase its volume, or (c) push the rear cap and contribute to central breakup. In conventional T-junctions, there is no pathway (b), and (a) is negligible at higher \( Ca \). In the lateral breakup-enabled T-junctions, the pathway (a) may be enhanced by an enlarged “gutter” area of the continuous phase when \( Ca \) is high (prominent for high aspect ratio channel [33]). Together with the uniquely presented pathway (b), it indicates that the lateral breakup-enabled T-junction uses a smaller portion of the incoming flow for central breakup compared to a conventional T-junction. This means for the same droplet length \( L_o \), a higher \( Ca^*_o \) is required to enable the central breakup and the transition, reflected by the increased constant \( (Ca_oL_o)^* \). In Figure 5 we maps the breakup regimes near the transition zone for four geometries with the same outlet widths in a logarithmic scale (From geometries A,B,D and E described in the Table). The decay rate of \( Ca^*_o \) with \( L_o \) is similar for all the tested geometries, as a power law with an exponent close to -1, similar to the above observation. The intersect of these -1 laws, proportional to the constant \( (Ca_oL_o)^* \), varies among the geometries. Geometries with more prominent lateral breakup (higher value of \( \beta \)) require a higher \( Ca^*_o \) to recover central breakup.

We also mention that the geometry may alter the relative time scale of the two processes. For example, on geometries that favor less the lateral breakup (e.g. geometry B), there is no lateral/central simultaneous breakup near the transition region, as shown in Figure 5a for geometry A, indicating a much slower lateral breakup at this moment than the central breakup. We thus warn that it is not impossible to have a lateral breakup process terminating before the central breakup process (of droplet flattening, concaving and finally pinching off), provided that a geometry promotes the former to have its process finished earlier. In a nutshell, the droplet breakup fate in these novel T-junctions should be determined by the temporal dynamics of both breakup processes and is dominated by the faster one. This means the two most common droplet formation mechanisms in microfluidics- driven by hydrodynamic force and driven by surface tension, simultaneously compete in the same geometry. By merely shifting flow condition, the droplet size and/or composition can be changed on-fly (Figure 6).

IV. CONFERENCE AND OUTLOOK

In summary, we reported on a novel lateral droplet breakup occurring in microfluidic T-junctions which leads to the formation of three daughter droplets. We experimentally evidenced that this new regime arises from an unbalanced capillary pressure at the drop interface induced by the strong gradient of confinement across the junction (provided that \( h > w_i > w_o \)). A geometrical design rule was proposed accordingly to enable the lateral breakup regime. We also developed a model depicting the development of the lateral pockets responsible for the ultimate lateral breakup, for low capillary number \( Ca \). Furthermore, we showed that a unique central breakup is recovered at higher \( Ca \), a mechanism observed in conventional T-junction. We showed that the critical capillary number \( Ca^* \) marking this transition from lateral to central breakup is compatible with an inverse dependency on the droplet length. The presence of the lateral pockets and their inflation explains that the values of \( Ca^* \) are orders of magnitude higher than predicted by a scaling analysis in the spirit of Haringa et al. [44]. Accounting for a thickening of the gutter at higher
**FIG. 6.** Different daughter droplet composition from each droplet breakup event, with geometry B. From top to bottom: increasing the number of daughter droplets (by decreasing the capillary number $Ca$). From left to right: increasing the daughter droplet size and/or size ratio (by increasing the droplet length $L_o$). The scale bar represents 100 µm.

$Ca$, as observed by Lozar et al. [53], was not sufficient to explain high values of $Ca^*$ reported. A thorough theoretical determination of $Ca^*$ remains to be achieved and is a challenge for future studies.

In the end, both hydrodynamic-force-driven and surface-tension-driven mechanisms are enabled on one geometry which allows new microfluidics functionalities. On one hand, active control over the flow condition can change droplet composition and sizes without changing geometries; On the other hand, without active control, the mere change of the content or property of the droplet could possibly alter the temporal competition of the two breakup regimes thus shifting the breakup results for passive applications. Altogether, we expect that these new breakup phenomena will provide versatile tools to the community to manipulate and control the volume of droplets.

**APPENDIX A - MATHEMATICAL MODELLING OF THE INFLATION OF THE LATERAL POCKETS AT LOW $Ca$**

Hereafter, we fully characterize the inlet and outlet gutters regime of the droplet (shown in Figure 3a), as they couple with equation (7) and (9) for the pocket dynamic through the boundary conditions and the conservation of the droplet volume. We then show that they constitute altogether a closed system that is made non-dimensional, and after some mathematical rearrangements, can be directly integrated in time.

Let $R_g^{(i)}(s,t)$ designate the radius of the gutter in the inlet channel (see Figure 3a) whose internal coordinate is $s \in [0; L_i(t)]$, purely along the $x$ direction. Solving eq.(4) subject to $R_g^{(i)}(0,t) = F_i$ leads to

$$R_g^{(i)}(s,t)^3 = F_i^3 - q_i(t)As$$

where $q_i(t)$ is the inlet gutter flow rate. By continuity, we can express it in terms of $k(\eta,t)$ using eq.(8) as

$$q_i(t) = \frac{4\gamma}{r_{h,S}[z(0,t) = h/2]} \frac{\partial k(0,t)}{\partial \eta},$$

(we recall that $\eta = 0$ designates the opening of the pocket at the junction and $\eta = L_p(t)$ its closure (see Figure 3a).)

The four boundary conditions for $z(\eta,t)$ and $k(\eta,t)$ write $z(0,t) = z(L_p(t),t) = h/2$, $k(0,t) = 1/R_g^{(i)}(L_i(t),t) - 2/w_o$, and $k(L_p(t),t) = 0$. The outlet gutter, of length $L_o(t)$ (see Figure 3a), has a radius $R_g^{(o)}(\alpha,t)$ whose internal coordinate is $\alpha \in [0; L_o(t)]$, purely along the $y$ direction. The radius $R_g^{(o)}(\alpha,t)$ is characterized by solving eq.(4) subject to $R_g^{(o)}(0,t) = w_o/2$ (since $k(L_p(t),0) = 0$) :

$$R_g^{(o)}(\alpha,t)^3 = \left(\frac{w_o}{2}\right)^3 - q_o(t)A\alpha, \quad \text{where} \quad q_o(t) = \frac{4\gamma}{r_{h,S}[z(L_p(t),t) = h/2]} \frac{\partial k(L_p(t),t)}{\partial \eta}$$
Its length \( L_o(t) \) is easily determined by imposing \( R_g^{(o)}(L_o(t), t) = F_o \). As will become clear in a moment, the problem is closed by imposing of conservation of the total volume of the droplet. From now on quantities are made non-dimensional, by \( h \) in space and \( \mu h/\gamma \) in time

\[
h(\tilde{s}, \tilde{\eta}, \tilde{\alpha}) = (s, \eta, \alpha), \quad \frac{\mu h}{\gamma} \tilde{t} = t, \quad h^2 \tilde{S} = S, \quad \frac{h^2 \gamma}{\mu} \tilde{q} = q, \quad \frac{1}{h} \tilde{k} = k, \quad h \tilde{z} = z,
\]

\[
\frac{\mu}{h^2} \tilde{r}_{h,s} = r_{h,s}, \quad \text{and} \quad \frac{\gamma}{\mu} Ca = U.
\]

Equations (7) and (9) thus non-dimensionalized, they are then put in the form of a classical conservation law for \( \tilde{z}(\tilde{\eta}, \tilde{t}) \) and \( \tilde{k}(\tilde{\eta}, \tilde{t}) \):

\[
\begin{bmatrix}
1 & 0 \\
0 & 0
\end{bmatrix} \frac{\partial}{\partial \tilde{t}} \begin{bmatrix} \tilde{z} \\ \tilde{k} \end{bmatrix} + \frac{\partial}{\partial \tilde{\eta}} \begin{bmatrix}
-\frac{B}{r_{h,s}} \tilde{z} - \frac{1}{\tilde{L}_p} \frac{\partial \tilde{k}}{\partial \tilde{\eta}} \\
- \frac{1}{\tilde{L}_p} \frac{\partial \tilde{k}}{\partial \tilde{\eta}} \left[ 1 + \left( \frac{1}{\tilde{L}_p} \right)^2 \right]^{-1/2}
\end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}, \quad \text{for} \quad 0 \leq \eta \leq L_p(t)
\]

(13)

where all the tildes have been dropped and \( B = 1/w_o \) is a constant (it is understood that \( L_p \) and \( w_o \) have been made non-dimensional by \( h \), etc.). System (13) is re-written under the change of variable \( \xi = \eta/L_p(t) \) in order to be solved over the time-independent domain \( 0 \leq \xi \leq 1 \), which is significantly more convenient. The partial derivatives are transformed as \( \partial_t \to \partial_t - (\partial_t L_p) L_p^{-1} \partial_\xi \) and \( \partial_\eta \to \partial_{L_p}^{-1} \partial_\xi \):

\[
\begin{bmatrix}
1 & 0 \\
0 & 0
\end{bmatrix} \frac{\partial}{\partial \tilde{t}} \begin{bmatrix} \tilde{z} \\ \tilde{k} \end{bmatrix} + \frac{\partial}{\partial \tilde{\xi}} \begin{bmatrix}
-\frac{dL_p}{dt} \tilde{L}_p^{-1} \tilde{z} - \frac{1}{\tilde{L}_p} \frac{\tilde{k}}{\tilde{L}_p} \\
- \frac{1}{\tilde{L}_p^2} \frac{\tilde{k}}{\tilde{L}_p} \left[ 1 + \left( \frac{1}{\tilde{L}_p} \right)^2 \right]^{-1/2}
\end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}
\]

(14)

where \( z(\eta, t) = \tilde{z}(\xi, t) \), then \( k(\eta, t) = \tilde{k}(\xi, t) \). Under this change of variables the flow rate \( q(\eta, t) = \tilde{q}(\xi, t) \) occurring inside the pocket, and the flow rates \( q_i(t) \) and \( q_o(t) \) occurring inside the inlet and outlet gutters, respectively, express:

\[
\tilde{q}(\xi, t) = \frac{4}{r_{h,S} [\tilde{z}(\xi, t) L_p(t)]} \frac{\partial \tilde{k}}{\partial \xi}, \quad q_i(t) = \tilde{q}(0, t), \quad \text{and} \quad q_o(t) = \tilde{q}(1, t).
\]

The boundary conditions of system (14) are re-written:

\[
\begin{align*}
\tilde{z}(0, t) &= 1/2, \quad \tilde{z}(1, t) = 1/2, \\
\tilde{k}(0, t) &= \left[ (F_i^3 - q_i(t) A L_i(t))^{-1/3} - \frac{2}{w_o} \right], \quad \text{and} \quad \tilde{k}(1, t) = 0.
\end{align*}
\]

(15)

(with the non-dimensional \( A = 3C/(4 - \pi) \)). A third equation is necessary for the third unknown \( L_p(t) \), and the problem is closed by imposing the volume conservation \( V(t) = V(0) \). Let \( V_g^{(i)}(t) \) designate the volume of the part of the droplet contained in the inlet channel and where a gutter is present (i.e. for \( 0 \leq \xi \leq L_i(t) \)) ; the volume of the rear cap is in addition \( V_g^{(o)}(t) \). Accordingly, let \( V_g^{(o)}(t) \) be the volume of the part of the droplet contained in one of the two outlet channels and where a gutter is present (i.e. for \( 0 \leq \xi \leq L_o(t) \)) ; the volume of one front cap is in addition \( V_g^{(c)} \). We recall that the expression for the cross sectional area of the discrete phase in the pocket region is \( S[z(\eta, t)] = (\pi - 4) w_o^2 / 4 + 2 w_o \tilde{z}(\eta, t) \), such that it is associated to a volume contribution in a outlet channel of \( \int_0^{\eta=L_o(t)} S[z(\eta, t)] d\eta \). Eventually:

\[
V(t) = 2 V_g^{(o)} + V_g^{(i)}(t) + V_g^{(i)}(t) + 2 V_g^{(o)}(t) + 2 \int_0^{\eta=L_o(t)} S[z(\eta, t)] d\eta
\]

\[
= 2 V_g^{(o)} + V_g^{(i)}(t) + V_g^{(i)}(t) + 2 V_g^{(o)}(t) + 2 L_p(t) \left[ \frac{(\pi - 4) w_o^2}{4} + 2 w_o \int_0^1 \tilde{z}(\xi, t) d\xi \right] = V(0)
\]

(16)

In addition, the cross sectional area the drop in a region where a gutter (of radius \( R_g \)) is present is \( S_g^{(i,o)} = h w_{i,o} - \left( R_g^{(i,o)} \right)^2 (4 - \pi) \), such that
by the rear cap volume $V_{\text{cap}}$. This leads to:

$$V_g^{(i)}(t) = h w_i L_i(t) - \frac{3(4 - \pi)}{5 A q_i(t)} \left[ F_i^5 - (F_i^3 - L_i(t) A q_i(t))^{5/3} \right]$$

In order to mimic a constant-velocity progression of the droplet in the inlet channel before the rear droplet interface reaches the junction, as observed experimentally, the length $L_i(t)$ is chosen as a ramp in time

$$L_i(t) = \begin{cases} L_i(0) - 0.85 \cdot t \cdot Ca & \text{if } 0 \leq t \leq t_J \\ 0 & \text{if } t \geq t_J \end{cases}$$

which acts as a source of excitation for the system [14] through the boundary condition for $k(0, t)$ in (15). At the time $t_J = L_i(0)/(0.85Ca)$ the rear droplet interface reaches the junction, and $L_i(0)$ is such that the necking condition as shown in Figure 3b is met. The coefficient 0.85 multiplying $Ca$ arises from the experimental data (shown in Figure 3b). The rear cap volume and curvature need also to be treated differently depending on whether $t$ is smaller or larger than $t_J$: let $V_{\text{cap}}[h, w_i]$ designate the equilibrium volume of the rear cap, whose value is taken from Musterd et al. [54] for $H/W \leq 1$

$$A_{bd}[H, W] = HW - 4 \cdot F[W, H]^2(1 - \pi/4) = HW + F[W, H]^2(\pi - 4)$$

$$L_{\text{cap}}[H, W] = \frac{W}{2}$$

$$V_{\text{cap}}[H, W] = \int_0^{L_{\text{cap}}} A_{bd}[H, W] \left( 1 - \frac{y^2}{L_{\text{cap}}[H, W]^2} \right) dy = \frac{2}{3} L_{\text{cap}}[H, W] A_{bd}[H, W]$$

Thereby the rear cap volume $V_{\text{cap}}^{(i)}(t)$ is implemented as

$$V_{\text{cap}}^{(i)}(t) = \begin{cases} V_{\text{cap}}[h, w_i] = \text{cst} & \text{if } 0 \leq t \leq t_J \\ V_{\text{cap}}[h, w_i] \frac{C_i(t)}{w_o} & \text{if } t \geq t_J \end{cases}$$

, where $C_i(t)$ is the rear cap curvature with $C_i(t \leq t_J) = \kappa_i$. Above $t = t_J$, the rear droplet interface must undergo the incoming flow rate $h w_i Ca$ and the following equation for the cap volume is activated

$$\frac{d V_{\text{cap}}^{(i)}}{dt} = q_i(t) - Ca h w_i$$

Injecting (18) in (19) leads to an evolution equation for $C_i(t)$ for $t \geq t_J$, and the boundary condition for the curvature at the opening of the pocket is accordingly replaced by $k(0, t) = C_i(t) - 2/w_o$ for these times.

**APPENDIX B - A SCALING ARGUMENT FOR ONSET OF CENTRAL BREAKUP**

In the spirit of reference [44], we try to obtain a scaling of the critical capillary number for central breakup to happen. Neglecting the presence of a lateral inflating pocket, the inversely proportional relationship between $C_a$ and $L_o/w_o$ might be understood as follows: after the body of the droplet has fully entered the outlet channels, we consider a threshold situation where the rear cap is flat for the observer, such that the rear cap curvature is assumed $1/F_i = 2/h$, although the precise value of the latter has little influence on the scaling law derived hereafter. The threshold capillary number above which a central breakup (CB) is expected is obtained by balancing the continuous flow rate arriving in the junction ($C_a w_i h$), with the capillary flow rate in the four gutters located in the outlet channel $(4(1/F_o - 2/h)/(r_o L_o))$, the quantity $r_o$ being the hydraulic resistance per unit length of a gutter in the outlet channel. This leads to:

$$\frac{w_o}{w_i} C_a \sim \frac{4 w_o}{w_i^2 h r_o L_o} \left( \frac{1}{F_o} - \frac{2}{h} \right) \propto \left( \frac{L_o}{w_o} \right)^{-1}$$

(20)
For, \( w_o = 14/62, \ w_i = 30/62, \ h = 1 \) and using eq.\([1]\) for \( F_o \) and eq.\([3]\) with \( R_g = w_o/2 \) for \( r_o \), we obtain
\[
4 \left( \frac{1}{r_o} - \frac{2}{n} \right) / (w_o^2 h r_o) \approx 5 \cdot 10^{-5}.
\]
However, this corresponds to a \( w_o/w_i C^*_a \) approximately four orders of magnitude smaller than experimental values.

[1] L. Shang, Y. Cheng, and Y. Zhao, Emerging droplet microfluidics, Chem. Rev. 117, 7964 (2017).
[2] P. Zhu and L. Wang, Passive and active droplet generation with microfluidics: a review, Lab Chip 17, 34 (2017).
[3] M. Joanicot and A. Ajdari, Droplet control for microfluidics, Science 309, 887 (2005).
[4] A. C. Sun, D. J. Steyer, A. R. Allen, E. M. Payne, R. T. Kennedy, and C. R. Stephenson, A droplet microfluidic platform for high-throughput photochemical reaction discovery, Nat. Comm. 11, 1 (2020).
[5] Z. Swank, G. Michielin, H. M. Yip, P. Cohen, D. O. Andrey, N. Vuilleumier, L. Kaiser, I. Eckerle, B. Meyer, and S. J. Maerk, A high-throughput microfluidic nanoimmunoassay for detecting anti-sars-cov-2 antibodies in serum or ultralow-volume blood samples, Proc. Natl. Acad. Sci. 118 (2021).
[6] Y. Wang, R. Jin, B. Shen, N. Li, H. Zhou, W. Wang, Y. Zhao, M. Huang, P. Fang, S. Wang, et al., High-throughput functional screening for next-generation cancer immunotherapy using droplet-based microfluidics, Sci. Adv. 7, eabe3839 (2021).
[7] A. Kulesa, J. Kehe, J. E. Hurtado, P. Tawde, and P. C. Blainey, Combinatorial drug discovery in nanoliter droplets, Proc. Natl. Acad. Sci. 115, 6685 (2018).
[8] B. Schuster, M. Junkin, S. S. Kashaf, I. Romero-Calvo, K. Kirby, J. Matthews, C. R. Weber, A. Rzhetsky, K. P. White, and S. Tay, Automated microfluidic platform for dynamic and combinatorial drug screening of tumor organoids, Nat. Comm. 11, 1 (2020).
[9] N. G. Durmus, S. Tasoglu, and U. Demirci, Functional droplet networks, Nat. Mat. 12, 478 (2013).
[10] Y. Zhang, Z. Dong, C. Li, H. Du, N. X. Fang, L. Wu, and Y. Song, Continuous 3d printing from one single droplet, Nat. Comm. 11, 1 (2020).
[11] R. K. Kumar, T. A. Meiller-Legrand, A. Alcinesio, D. Gonzalez, D. A. Mavridou, O. J. Meacock, W. P. Smith, L. Zhou, W. Kim, G. S. Puell, et al., Droplet printing reveals the importance of micron-scale structure for bacterial ecology, Nat. Comm. 12, 1 (2021).
[12] C. M. Hindson, J. R. Chevillet, H. A. Briggs, E. N. Gallichotte, I. K. Ruf, B. J. Hindson, R. L. Vessella, and M. Tewari, Absolute quantification by droplet digital pcr versus analog real-time pcr, Nature Methods 10, 1003 (2013).
[13] Y. Zhang, Y. Minagawa, H. Kizoe, K. Miyazaki, R. Iino, H. Ueno, K. V. Tabata, Y. Shimane, and H. Noji, Accurate high-throughput screening based on digital protein synthesis in a massively parallel femtoliter droplet array, Sci. Adv. 5, eaaq1815 (2019).
[14] D. Zaremba, S. Bloński, and P. M. Korczyk, Integration of capillary–hydrodynamic logic circuitries for built-in control over multiple droplets in microfluidic networks, Lab Chip 21, 1771 (2021).
[15] A. I. Segaliny, G. Li, L. Kong, C. Ren, X. Chen, J. K. Wang, D. Baltimore, G. Wu, and W. Zhao, Functional tcr t cell screening using single-cell droplet microfluidics, Lab Chip 18, 3733 (2018).
[16] M. Pellegrino, A. Sciambi, S. Treusch, R. Durruthy-Durruthy, K. Gokhale, J. Jacob, T. X. Chen, J. A. Geis, W. Oldham, J. Matthews, et al., High-throughput single-cell dna sequencing of acute myeloid leukemia tumors with droplet microfluidics, Genome Res. 28, 1345 (2018).
[17] M. J. Spindler, A. L. Nelson, E. K. Wagner, N. Oppermans, J. S. Bridgeman, J. M. Heather, A. S. Adler, M. A. Asensio, R. C. Edgar, Y. W. Lim, et al., Massively parallel interrogation and mining of natively paired human tcra β repertoires, Nat. Biotechnol. 38, 609 (2020).
[18] A. Gérard, A. Woolfe, G. Mottet, M. Reichen, C. Castrillon, V. Menrath, S. Ellouze, A. Poitou, R. Doineau, L. Briseno-Roa, et al., High-throughput single-cell activity-based screening and sequencing of antibodies using droplet microfluidics, Nat. Biotechnol. 38, 715 (2020).
[19] T. Thorsen, R. W. Roberts, F. H. Arnold, and S. R. Quake, Dynamic pattern formation in a vesicle-generating microfluidic device, Phys. Rev. Lett. 86, 4163 (2001).
[20] S. L. Anna, N. Bontoux, and H. A. Stone, Formation of dispersions using “flow focusing” in microchannels, Appl. Phys. Lett. 82, 364 (2003).
[21] C. Cramer, P. Fischer, and E. J. Windhab, Drop formation in a co-flowing ambient fluid, Chem. Eng. Sci. 59, 3045 (2004).
[22] J. H. Xu, S. Li, J. Tan, and G. Luo, Correlations of droplet formation in t-junction microfluidic devices: from squeezing to dripping, Microfluid. Nanofluid. 5, 711 (2008).
[23] C. N. Baroud, F. Gallaire, and R. Dangla, Dynamics of microfluidic droplets, Lab Chip 10, 2032 (2010).
[24] P. M. Korczyk, V. Van Steijn, S. Bloński, D. Zaremba, D. A. Beattie, and P. Garstecki, Accounting for corner flow unifies the understanding of droplet formation in microfluidic channels, Nat. Comm. 10, 1 (2019).
[25] R. Dangla, E. Fradet, Y. Lopez, and C. N. Baroud, The physical mechanisms of step emulsification, J. Phys. D 46, 114003 (2013).
[26] M. De Menech, P. Garstecki, F. Jousse, and H. A. Stone, Transition from squeezing to dripping in a microfluidic t-shaped junction, J. Fluid. Mech. 595, 141 (2008).
[27] R. Dangla, S. C. Kayi, and C. N. Baroud, Droplet microfluidics driven by gradients of confinement, Proc. Natl. Acad. Sci. et al.
110, 853 (2013).
[28] Z. Li, A. Leshansky, L. Pismen, and P. Tabeling, Step-emulsification in a microfluidic device, Lab Chip 15, 1023 (2015).
[29] M. L. Eggersdorfer, H. Seybold, A. Ofner, D. A. Weitz, and A. R. Studart, Wetting controls of droplet formation in step emulsification, Proc. Natl. Acad. Sci. 115, 9479 (2018).
[30] X. Niu, F. Gielen, J. B. Edel, and A. J. Demello, A microdroplet dilutor for high-throughput screening, Nat. Chem. 3, 437 (2011).
[31] F. Lan, J. R. Haliburton, A. Yuan, and A. R. Abate, Droplet barcoding for massively parallel single-molecule deep sequencing, Nat. Comm. 7, 1 (2016).
[32] D. Link, S. L. Anna, D. Weitz, and H. Stone, Geometrically mediated breakup of drops in microfluidic devices, Phys. Rev. Lett. 92, 054503 (2004).
[33] M. De Menech, Modeling of droplet breakup in a microfluidic t-shaped junction with a phase-field model, Phys. Rev. E 73, 031505 (2006).
[34] A. M. Leshansky and L. M. Pismen, Breakup of drops in a microfluidic t junction, Phys. Fluids 21, 023303 (2009).
[35] X. Niu, F. Gielen, J. B. Edel, and A. J. Demello, A microdroplet dilutor for high-throughput screening, Nat. Chem. 3, 437 (2011).
[36] F. Lan, J. R. Haliburton, A. Yuan, and A. R. Abate, Droplet barcoding for massively parallel single-molecule deep sequencing, Nat. Comm. 7, 1 (2016).
[37] D. Link, S. L. Anna, D. Weitz, and H. Stone, Geometrically mediated breakup of drops in microfluidic devices, Phys. Rev. Lett. 92, 054503 (2004).
[38] M. De Menech, Modeling of droplet breakup in a microfluidic t-shaped junction with a phase-field model, Phys. Rev. E 73, 031505 (2006).
[39] A. M. Leshansky and L. M. Pismen, Breakup of drops in a microfluidic t junction, Phys. Fluids 21, 023303 (2009).
[40] X. Niu, F. Gielen, J. B. Edel, and A. J. Demello, A microdroplet dilutor for high-throughput screening, Nat. Chem. 3, 437 (2011).
[41] F. Lan, J. R. Haliburton, A. Yuan, and A. R. Abate, Droplet barcoding for massively parallel single-molecule deep sequencing, Nat. Comm. 7, 1 (2016).
[42] D. Link, S. L. Anna, D. Weitz, and H. Stone, Geometrically mediated breakup of drops in microfluidic devices, Phys. Rev. Lett. 92, 054503 (2004).
[43] M. De Menech, Modeling of droplet breakup in a microfluidic t-shaped junction with a phase-field model, Phys. Rev. E 73, 031505 (2006).
[44] A. M. Leshansky and L. M. Pismen, Breakup of drops in a microfluidic t junction, Phys. Fluids 21, 023303 (2009).
[45] X. Niu, F. Gielen, J. B. Edel, and A. J. Demello, A microdroplet dilutor for high-throughput screening, Nat. Chem. 3, 437 (2011).
[46] F. Lan, J. R. Haliburton, A. Yuan, and A. R. Abate, Droplet barcoding for massively parallel single-molecule deep sequencing, Nat. Comm. 7, 1 (2016).
[47] D. Link, S. L. Anna, D. Weitz, and H. Stone, Geometrically mediated breakup of drops in microfluidic devices, Phys. Rev. Lett. 92, 054503 (2004).
[48] M. De Menech, Modeling of droplet breakup in a microfluidic t-shaped junction with a phase-field model, Phys. Rev. E 73, 031505 (2006).