Stereoscopic TR PIV measurement and POD analysis of flow behind the turbine prototype of model size

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Abstract. When measuring turbine prototype flow, a number of modes with different flow rates and cavitating vortex rope settings have been measured. The turbulent flow in the draft tube of diameter 240 mm reaches the Reynolds number of $10^5$. The vortex and highly swirling flow is developed in the draft tube. The usage of kHz-order frame rates was necessary to resolve the velocity field. The investigated area in the mixing vessel was examined by the stereoscopic time-resolved PIV technique. Further mode evaluation allows comparison of cross-sectional velocities in the vector map. The Proper orthogonal decomposition analysis was applied on 3D vector maps, those including u, v, w velocity compounds. In the selected regimes – operating points with volume flow rate 97 l/sec and 114 l/sec, the greatest risk of transition to cavitation mode was identified, so they were studied in detail.

1 Introduction

The development of energy storage resources is a response to weather fluctuations and growth of green power plants (solar and wind power). There raises an urgent need for energy storage and its use depending on the immediate increase. It is also very closely connected with ensuring the safety and stability of the distribution system. The most effective functions are assured by pumped-storage hydroelectric power plants (PVE). The unique feature is their rapid response to the needs of the transmission network and the ability to ensure their re-commissioning in case of blackout. In Europe, most of the PVEs were built more than 20 years ago, i.e. before volatile renewable resource boom, where the requirements for dynamic PVE functions and bandwidth were less demanding than today. The number of PVEs installed in Asia and South America has been so far inadequate. The usage of conventional reverse turbines in off-optimal modes brings an unstable closed flow causing the vibration pulsation of the turbocharger. It forces the limitation of the working scope.

The progress in turbine optimization is in a design of new shape of the hydraulic parts of the reverse turbine, assuming the rotation of the fluid in the draft and suction tube. The design of impeller, draft and suction tube of reverse (pump) turbine with an extended operating band is based on computational modelling (CFD, mathematical optimization).

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Validation of models can be performed by advanced experimental techniques (time-
resolved PIV, tomography, high speed visualization).

The intention in progression is to suppress pulsations, which are the result of the cavity
of the swirling head. The novelty of the reverse turbine design is in optimization of the
plant as a whole unit (impeller plus suction unit) using computational modelling with help
of advanced experimental techniques. The solution is based on a thorough theoretical
analysis on stability and flow dynamics. The verification of the prototype runs in testing
room on a reverse turbine prototype. This prototype meets requirements and demands of
dynamic control function, thereby increasing the safety and resilience of the distribution
network.

The validation of the numerical calculations should be done by the method that allows
nonintrusive contactless measurement of fluid flow meeting the temporal resolution of an
unsteady flow. The turbulent flow in the draft tube of diameter 240 mm reaches the
Reynolds number of $10^5$. The vortex and highly swirling flow is developed in the draft tube.
The usage of kiloHertz-order frame rates was necessary to resolve the velocity field.
Another condition influencing the selection of the appropriate measuring methodology was
the 3D character of flow. The flow behind the turbine is anisotropic. The velocity
component in the mainstream direction greater then swirl flow. The time-resolved PIV (TR
PIV) can provide access to spatial - temporally varying flow fields at sampling rates of
kHz. The mainstream time-mean velocity was calculated from volume flowrate as
$W_0 = 2 \text{ m/s}$ and the velocities in swirl flow were expected as $U_0 \text{ and } V_0 \approx 0.3 \text{ m/s}$.
Measurement in two planes was impossible for spatial reasons and optical approach to the
prototype. Therefore, a one-off measurement was provided to get information on all three
velocity flow components. Confirming the expectations was to use stereo PIV system setup
know from conventional PIV system. Here, we set the stereo TR PIV (3D TR PIV) system
on Nd:YLF laser Litron running on maximal flashing frame 1kHz in double frame mode
and two high speed cameras set in 3D geometrical arrangement using Scheimpflug mounts.
The results of fluid flow presented in this paper are complemented by proper orthogonal
decomposition calculated for three velocity components [1-7].

2 Experimental Method

The selection of the measuring methodology and experiment conditions on the turbine
prototype were determined by the high Re number (Re > $10^5$) and the anisotropic character
of the fluid flow in the draft tube. The diameter of draft tube at the measuring plane was
240 mm. Average expected water flow through the cross section was 100 l/sec.

The time – resolved PIV extended with two high speed cameras to obtain stereo records
of fluid flow was suitable solution for monitoring of three velocity component using two
optical accesses. The experimental measurement was run in the test hall on the turbine
prototype. Together with the design of the geometric arrangement of the cameras and the
laser, it was necessary to design a suitable optical approach and to supplement the tube with
the optic extensions. According to requirements of optical measuring methods, the
prototype of suction and draft tube was manufactured with Plexiglas to ensure optical
access also for purpose of visualizations. It was mainly the reduction of the distortion
caused by the transition of light through various environments (water, Plexiglas, air) and
curved walls of draft tube.
caused by the transition of light through the laser, it was necessary to design a suitable optical approach and to supplement the prototype with optical accesses.

The diameter of the draft tube at the measuring plane was 240 mm. The selection of the measuring methodology and experimental techniques was motivated by the need to monitor the velocity flow components. Confirming the expectations was the usage of stereo Veloplot (3D TR PIV system) to provide access to spatially resolved PIV, which is an advanced experimental tool for the nonintrusive, contactless measurement of fluid flow meeting the temporal resolution requirements of the reverse turbine design. The novelty of the reverse turbine design is the usage of kiloHertz laser pulses to suppress pulsations of the swirling head. The vortex and highly swirling flow is developed in the draft tube.

The experimental measurement was carried out in the domain of the reverse turbine design. The mainstream time mean velocity was calculated from volume flowrate as $V_0 = \frac{Q}{A}$, where $Q$ is the flow rate and $A$ is the cross-sectional area.

The Reynolds number of the unsteady flow. The turbulent flow behind the turbine is anisotropic. The velocity flow in the mainstream direction is greater than the swirl flow. The time increases the particle density and illumination.

2.1 Measurement Technique Setup

The investigated area in the mixing vessel was examined by the time-resolved PIV technique. The stereocraphic TR PIV system was built on two high speed Speedsense cameras, complete with a sync module and a Litron Ld:Y300 pulse laser operation on the frequency 1 kHz. This kind of double cavity laser emits pulses of energy reaching 15 mJ in each pulse on wavelength 527 nm. The laser beam was extended into the vertical plane with cylindrical optics to reach the parameter of the planar laser sheet of thickness 1 mm and spread into the 300 mm width. The investigated area's diameter was 240 mm.

The two high speed cameras SpeedSense working on frequency 1kHz with resolution of (1280 x 800) px in double frame mode were equipped with low-passing filters to eliminate the backward flashes from the laser sheet that arises on the blades surfaces. The wavelength of the optical filter corresponds with the emitted light of the particles. The set of lens system Nikkon f/2.8 60 mm was also used. The cameras were fitted into optical amounts to reach Scheimpflug condition. Conventional particle image velocimetry uses a single camera oriented orthogonally to the illuminated plane. Stereoscopic simultaneous views from two different off-axis directions provide sufficient information to extract the out-of-plane and in-plane velocity components. We used the angular-displacement method in our experimental camera setup. That means that two cameras axes are not parallel, but rotated inward such that they intersect at the midpoint of the domain to be recorded. The object plane is not parallel to the lens plane Therefore it becomes difficult to obtain particles images that are well focused across the image plane. Most simple solution is to increase the depth of field of the recording optics. The depth of field $dof = \frac{4(1 + M^{-1})^2 f^2 \lambda}{\pi}$, where $M$ is the camera magnification, $f$ is the f-number, and $\lambda$ is the wavelength of the illuminating laser. A large depth of field can be obtained of increasing the f-number, implying that a smaller fraction of the light scattered by the particle will reach the camera. The second method to obtain images in focus over the entire image plane is to enforce the Scheimpflug condition. That requires the object plane, the lens plane, and the image plane are collinear. We used both methods with regard to insufficient saturation in our experiment.

The exposition time for both cameras operated on 330 usec. The increase of exposure time increases the particle density and illumination.
The laser and camera system was synchronized via timer box and controlled from the DantecStudio software. The expectation of the maximum frequency of the vortex structures was in tens of Herz. According to Nyquist criterion of sampling frequency it was set 500 Hz. The dataset of 5000 images was captured. The raw images were also processed in this software.

The analyses of captured images run in three main categories. There were run pre-processing analysis, i.e. image masking, image algorithm for blur and light reflection reduction. There was run the dewarping algorithm with the calibration function. The pre-processed images were analysed using standard cross-correlation method with interrogation area size (32 x 32) px and overlap 50%. The raw vector maps were validated with peak and range validation methods to obtain correct dataset. For the purpose of overview of the complex flow behaviour the statistical evaluation and the turbulence index was calculated. The dynamically changing velocity field was analysed by the Proper Orthogonal Decomposition (POD) for identifying the energy fractions and partial vortex structures in the fluid flow.

2.2 Calibration

The stereoscopic TR PIV requires spatial calibration with a specially designed calibration target. The use of a calibration target with an accurate dot matrix also enables subsequent post processing of captured images and dewarping of local distortions.

Standard calibration of the stereo PIV system is performed by a traversing calibration target. The movement of the target in a closed floating waterway could not be realized, therefore a multi-level target method was chosen.

The calibration target was designed as a spatial matrix with regular point alternation in two planes. When designing a target, it was important to keep the square structure of both planes, which later defined the axial orientation. The designed round calibration target was manufactured using 3D printing method. This method enables precise two colour printing with high resolution. The appropriately designed target must have the following parameters: number of pixel points in the image 10 x 10, the ratio of the size of the main points to the image width of 1:50, the ratio of the main points to the central 1:1.5, and the ratio of the main point size and 1:1 layer spacing. The target was designed as white dots on a matt black background. The main dot size was 7 mm and the regular dot was 5 mm in diameter. The distance between dots was 20 mm and the plane distance was 4 mm.

Fig. 2. Calibration target with a diameter of 240 mm for measurement in the experimental track.

2.3 Seeding

Solution for seeding was first supposed to use a natural flow of saturation. This was especially content of impurities and bubbles that have proven themselves in the past. The advantage of natural saturation was more considerate to the device. There was a legitimate concern about blade damage and the deposition of particles in the system. There was a problem with the seeding of the fluid flow due to the spatial layout of two cameras to the laser plane from experimental point of view. Each camera records the
evaluated area at a different angle to the scattering angle on the particle. The problem was the diffusion of light at different angles. The bubbles show a backscatter of laser light. Solid particles, on the other hand, exhibit forward scattering. However, the natural impurity content was not sufficiently proportional for both cameras to record particles of sufficient intensity, notwithstanding the fact that two non-comparable seeding units (density, viscosity, reflection index) were captured. The stereoscopic TR PIV method is particularly sensitive to the quality of seeding, especially when it comes to high-speed recording with short exposure times and limited light power. These arguments outweighed concerns about the damage to the system, which was not proven later. The volume of 50 m³ (whole volume in the turbine, pipe system and reservoir) of water was to be seeded with 50 μm PA particles.

Camera 1 – forward scattering

Camera 2 – backward scattering

Fig. 3. Examples of seeding using presence of natural dust, impurities and bubbles, and addition of PA 50μm particles.

3 Results and Discussion

When measuring turbine prototype flow, a number of modes with different flow rates and cavitating cavity settings have been measured. This article lists results from two modes that are most prominent. There is a risk of an early transition to the cavitating character of the fluid flow (due to under pressure) for both operating modes. The impeller optimization design was based on the suppression of the cavitating whirl. In the selected regimes – operating points marked as 293 and 298, the greatest risk of transition was identified, so they were studied in detail.

Mode 293 was running at fluid flow 97 l/sec with a slight overpressure of 20 kPa. In this mode, the cavitating rope did not go into the gaseous phase, so it was possible to perform PIV measurements. By lowering the pressure of 20 kPa under atmospheric pressure, the core of the cavitating whirl changed the phase to the gas occupies a large part of the evaluated area. Condition for PIV measurements are harder to reach due the reflections and lack of seeding inside the cavitating rope. Mode 298 is characterized by a flow of 114 l/s at atmospheric pressure. This mode was stable under current operating conditions.

The stereoscopic model used to reconstruct three component vector maps was loaded with a number of limits. First and foremost, due to the complexity of the scene and the
views to the measured area, it was not possible to cover the entire cross-section of both cameras. In places where the view of a single camera is hidden, it is not possible to reconstruct the data properly. This leads to misinterpreted results, especially in some extreme areas. However, most of the cross-section is interpreted correctly and it is certainly possible to have the overall flow.

The basic evaluation of fluid flow behind turbine is time-averaged statistics (Figure 4). We captured in the following vector maps for following measurement points 293, and 298. The basic physical quantities of the operation were recorded at all of these measurement points.

![Vector maps of fluid flow behind the turbine prototype processed as 3D and 2D vector maps for regime a) 293, and b) 298.](image)

**Fig. 4.** Time-averaged statistics of fluid flow behind the turbine prototype processed as 3D and 2D vector maps for regime a) 293, and b) 298.

From the basic view of the vector maps, there is a difference in the mode at the measurement point 298. While in the other modes exhibits the dominant stream of water is in the peripheral regions, at the point 298 mode, the main stream with the vortex structure moves closer to the centre of the cross-section. The maximum velocity are higher in this mode, $w_{\text{max}} = 3m/s$. An interesting comparison of paragraphs 298 and 293 shows another difference in the characteristics of the modes.

There is a difference between rotations of the main current behind the impeller from this interpretation of the results (Figure 4). While in the modes at points 293 rotates the main current according to the direction of the impeller, in this case in the clockwise direction, the mode at point 298 rotates in the opposite direction of the impeller. This behaviour of the vortex structures was subsequently confirmed by high-speed visualizations in the presence of the gaseous component.

Further mode evaluation allows comparison of cross-sectional velocities in the vector map.
The Proper orthogonal decomposition analysis was applied on 3D vector maps, those including $u$, $v$, $w$ velocity compounds. It is a mathematical method that gains and clarifies the flow structures based on extracting a basis for modal decomposition from an ensemble of signals. [8] We can reconstruct flow field and demonstrate the influence of different flow structures by the selection of main dominant POD modes. The major POD modes that effects the dominant flow is seen in Figure 5. The POD Snapshot is based on autocorrelation function and depends on the number of instantaneous acquired samples acquired. We can see in figure 5 two dominant Modes that are significant for flow regime 293. For comparison to this we chose the first dominant mode even for the regime 298.

![POD Snapshots](image)

Fig. 5. POD Snapshots for regime 293, and 298 according to energy fractions.

The general aim of POD is to find the optimal representation of measured field realizations. The eigen functions are sometimes referred to coherent structures. The structures are highly correlated in an average sense with the flow field. The POD analysis was performed on 5 000 sequential 3D vector maps. The POD projection of Mode 1 and 2 for both regimes is seen in Figure 6 and Figure 7. These two dominant modes affect the resulting flow structure. The presentation of all three components of velocity, i.e. $u$, $v$ in plane and $w$ as vertical velocity component, is also evident in anisotropy and orientation of the main and swirl flow.

The interpretation of 3D vector velocity fields is difficult, especially if they are strongly anisotropic. In this experiment, the component of the vertical velocity $w$ was predominantly in the mainstream direction, so it follows the main swirl flow. We focused on viewing this folder, when interpreting data.

In regime 293, the centrifugal flow orientation is predominant, resulting in a structure with a maximum velocity in the laser plane ($u$, $v$ velocity components) – horizontal, near the walls. The rotational frequency of these structures is 7 Hz. The swirl structure and centred local velocity decrease is dominant in both POD modes. The return fluid flows in the centre time-averaged velocity statistics is created by averaging these vortex structures, which rotate with the main stream. The increase of velocity near the walls is well visible on the projection of 3D images in figure 6.

In regime 298 in POD mode 1, and in 2 prevail the vortex structures in the centre of swirl structure. Complex, irregularly structured vortex are projected into time-averaged vector statistics as two opposite vortex structures moving in counter clockwise direction of rotation. In averaged statistics, these partial vortex structures cause a uniform velocity profile as it is seen in figure 8. The occurrence of both POD modes is time-based as it is seen in figure 7. This local closure predicts the incidence of cavitation rope if pressure drop.
There is seen significant vortex breakdown. This breakdown is characterised by decrease of axial velocity along the axis, leading to internal stagnation point or even backflow [7].

Two modes differing in flow, achieve significant different flow characteristics, which are also reflected in the speed profile evaluation that was taken across the transverse region passing through the centre of the diffuser. According to the velocity profiles for vertical velocity component $w$ in Figure 8 can be watched the dominant trend of the flow reaches the maximum near the wall of the diffuser. Towards the centre of the diffusers, the velocity of the velocity decreases and there is a backward flow and significant closure in the horizontal plane.
Against this mode 298 towards the centre of the diffuser, the speed increases, including the rotary component, see vector map above. The small drop is due to the range behind the impeller's charge.

**Fig. 7.** POD 1st, and 2nd mode of flow structures in regime 298 and time history of POD coefficient for both modes.
4 Conclusion

The measurement in draft tube below the impeller was a technically demanding. In addition, it has to be solved with compensating optical elements. The distortion near the curved walls was too large to be able to measure the speed field in these areas. The evaluation of field speeds near the wall provides the most interesting results, especially in the area behind the rotating impeller, when the main current is closed.

Using optimized PIV stereo methods and high speed recordings, it was possible to monitor and evaluate this complex task as well. By application of the POD analysis, dominant vortex structures were detected, which were evaluated in the form of 3D graphs. The distinction between the two modes is reflected not only in the evaluation of the velocity profiles across the monitored area, but also in the resulting frequency analysis, where the dominant frequencies of the vortex structures can be detected. This measurement responds to the CFD simulation already conducted to optimize the turbine.

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