Solar constraints on captured electrophilic dark matter

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Abstract

Dark matter captured by interaction with electrons inside the Sun may annihilate via long-lived mediator to produce observable gamma ray signals. We utilize solar gamma ray flux measurements from the Fermi Large Area Telescope and High Altitude Water Cherenkov observatory to put bounds on the dark matter electron scattering cross-section. We find that our limits are four to six orders of magnitude stronger than the existing limits for dark matter masses ranging between GeV to PeV scale.

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1 Introduction

The gravitational wells of celestial bodies can act as local reservoirs for ambient dark matter (DM), making them attractive location in the sky to search for it. Typically the relic distributions of particulate DM may be gravitationally focused by the massive stars and subsequently undergo scattering with the stellar constituents dissipating energy in the process. If the resultant energy of the DM

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particle is below the escape energy, it gets captured within the astrophysical body [1–3]. Over time a
density of captured DM may build up in these celestial objects that are considerably higher than the
typical halo distribution making them DM hotspots in the sky.

Evidently the Sun remains the most significant and by far the most experimentally scrutinized star
in the sky making it a sensitive tool to study properties of captured DM [4–25]. While scattering
with solar nucleons is the major capture mechanism in the Sun [4–25]. Electrophilic DM particles can
instead scatter off solar electrons and get trapped. Such electrophilic DM captured in the Sun can
annihilate and produce detectable annihilation signatures owing to the local high density. Neutrino
signals from these annihilations have been considered in [26, 27]. If the DM particles annihilate
via long-lived mediators [8, 13, 14, 20–25, 28, 29], the decay of these escaped mediators can produce
detectable gamma ray signatures. In this paper, we demonstrate that the Fermi Large Area Telescope
(Fermi-LAT) [30–32] and High Altitude Water Cherenkov (HAWC) observatory [33] are sensitive to
such a photon flux. By comparing the solar gamma ray data from Fermi-LAT and HAWC with
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such a photon flux. By comparing the solar gamma ray data from Fermi-LAT and HAWC with
such a photon flux, we for the first time put constraints on DM-electron scattering cross-section at
O(10^{-43} – 10^{-40}) cm^2 for DM mass ranging from a few GeV to 1 PeV. These limits are ~ 4 – 6 orders
of magnitude stronger than the current bounds from the other considerations [26, 34].

2 Solar DM capture via electron scattering

The gravitationally focused DM particles can scatter with the electrons inside the Sun and get trapped.
The capture rate of DM particles is given by [27, 35]

\[ C_\odot = \left( \frac{\rho_\chi}{m_\chi} \right) \int_0^{R_\odot} dr \frac{4 \pi r^2}{4} \int_0^{u_{\text{esc}}} du_\chi \frac{f(u_\chi)}{u_\chi} \frac{w(r)}{u_\chi} \int_0^{v_{\text{esc}}(r)} dv \Omega^{-}(w(r) \rightarrow v), \]  

where \( \rho_\chi \) is the local DM density, \( f(u_\chi) \) is the velocity distribution profile of DM, \( m_\chi \) is mass of the
DM particle and \( R_\odot \) is the radius of the Sun, \( w(r) = \sqrt{u_\chi^2 + v_{\text{esc}}^2(r)} \) is the velocity of a gravitationally
focused DM particle at a distance \( r \) from the center of the Sun, \( v_{\text{esc}}(r) \) being the escape velocity at
that location. The galactic escape velocity of DM is given by \( u_{\text{esc}} = 528 \text{ km/s} \) [36,37]. The differential rate of DM-electron scattering that can trigger a velocity change from \( w(r) \) to \( v \) can be expressed as

\[ \Omega^{-}(w(r) \rightarrow v) = \frac{2}{\sqrt{\pi}} \left( \frac{m_\chi + m_e}{4m_\chi m_e} \right)^2 \frac{v}{w(r)} n_e(r) \sigma_{\chi e} \left[ \int_{-\alpha_+}^{\alpha_+} dy e^{-y^2} + e^{-\frac{m_\chi (w(r)^2 - v^2)}{2v_{\odot}(r)}} \int_{-\beta_-}^{\beta_+} dy e^{-y^2} \right], \]  

where \( m_e \) is the electron mass and \( \sigma_{\chi e} \) is the velocity independent DM-electron scattering cross-section. We have utilized the definition [2]

\[ \alpha_\pm = \sqrt{\frac{m_e}{2T_\odot(r)}} \left( \mu_\pm v \pm \mu_\pm w(r) \right), \]  

where \( \mu_\pm = \frac{m_\chi - m_e}{m_e} \pm 1 \), \( n_e(r) \) and \( T_\odot(r) \) are the electron number density and temperature profile of the
Sun [38]. A similar expression can be obtained for \( \beta_\pm = \alpha_\pm (\mu_\pm w \rightarrow \mu_\pm) \). As the Sun is moving with
a velocity \( v_{\odot} = 220 \text{ km/s} \) in the galactic halo of DM, the Maxwell-Boltzmann velocity distribution of
DM in the rest frame of the Sun is given by [27]

\[ f(u_\chi) = \frac{3}{2 \pi} \frac{u_\chi}{v_{\odot} v_d} \left( e^{-\frac{3(u_\chi - v_{\odot})^2}{2v_d^2}} - e^{-\frac{3(u_\chi + v_{\odot})^2}{2v_d^2}} \right), \]  

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where the DM velocity dispersion ($v_d$) is assumed to be $270 \text{ km/s}$. Electrons, being light particles, attain a significant thermal velocity within the solar interior which makes the inclusion of solar temperature profile crucial in determining the capture rate [27]. For the DM mass range we have explored in the work, the capture rate exhibits a secular decline with increasing mass.

Evidently a tree level coupling between the DM and the electron can model dependently generate radiative coupling between the DM and nucleon [26, 39]. This crucially depends on the lorentz structures of the tree level coupling and can be suppressed for specific choices [26]. These loop induced couplings would further enhance the capture rate making the limits on DM-electron couplings more stringent. We neglect these model dependent loop induced DM-nucleon couplings and consider conservative limits originating from pure DM-electron interactions.

3 Gamma ray flux

The number density of the captured DM inside the Sun is governed by the interplay of capture, annihilation, and evaporation. For heavier DM masses ($m_\chi \gtrsim 5 \text{ GeV}$), the evaporation becomes numerically insignificant [35, 40]. We assume equilibrium between the capture and annihilation of DM in the Sun that allows us to relate the annihilation with the capture rate as given below,

$$\Gamma_{\text{ann}} = \frac{1}{2} C_{\text{ann}} N_\chi^2 = \frac{C_\odot}{2},$$

(5)

where $C_{\text{ann}}$ is the coefficient of DM annihilation and $C_\odot$ denotes the capture rate defined in Eq. (1). This correlation makes our results independent of the annihilation cross-section. DM particles annihilate to SM states through mediator that has a sufficiently long lifetime ($\tau_Y$) or a large velocity boost ($\eta$) can escape from the solar environment ($L_Y = \eta c \tau_Y > R_\odot$). The mediator can decay to various SM final states which can give rise to observable photon flux at the Earth-based observatories [20–25]. The differential photon flux at the surface of Earth originating from such mediator is given by

$$E_\gamma^2 \frac{d\phi_\gamma}{dE_\gamma} = \frac{\Gamma_{\text{ann}}}{4\pi D_\odot^2} \times \text{Br}(Y \to \text{SM SM}) \times \left( E_\gamma^2 \frac{dN_{\gamma}}{dE_{\gamma}} \right) \times \left( e^{-\frac{R_\odot}{\eta c \tau_Y}} - e^{-\frac{D_\odot}{\eta c \tau_Y}} \right),$$

(6)

where $\text{Br}(Y \to \text{SM SM})$ is the branching ratio to a given SM final state, $D_\odot$ is the distance between the Sun and the Earth. The gamma ray spectrum, $dN_{\gamma}/dE_{\gamma}$, is adopted from [41]. The last term in the parenthesis estimates the survival probability of the signal to reach terrestrial detectors. Under equilibrium assumption, for a given decay route of the mediator, the photon flux for a specified DM and mediator mass is solely determined by the DM-electron scattering cross-section, $\sigma_{\chi e}$. Assuming 100% branching ratio, we present representative photon flux for various SM final states in Fig. 1. The lifetime of the mediator have a lower bound in the nano-second range from collider experiments [42] and upper limits from cosmological observations like BBN is $\lesssim 1 \text{ s}$ [43, 44]. These bounds are easily in consonance with the mediator considered here.

4 Results

State of the art solar gamma ray measurements in $0.1 - 10^3 \text{ GeV}$ energy range is provided by the Fermi-LAT satellite based experiment [30–32]. The Fermi-LAT solar gamma ray flux measurements [32] are
Figure 1: Photon flux reaching at the surface of Earth for different SM final states: $\gamma\gamma$ (red), $\tau\tau$ (gray), $b\bar{b}$ (purple) and $\mu\bar{\mu}$ (blue) for DM mass, $m_\chi = 20$ TeV, mediator mass, $m_Y = 50$ GeV and DM-electron scattering cross-section, $\sigma_{\chi e} = 10^{-40}$ cm$^2$ are portrayed. We have also depicted the solar gamma ray flux measurements from Fermi-LAT [32] and HAWC [33] with yellow and green histograms respectively.

shown in Fig. 1. It’s worth mentioning that the Fermi-LAT data in the last two bins are upper limits obtained from null measurements. The HAWC [33] and ARGO-YBJ [45] have looked for solar gamma rays in the multi-TeV window, which complement the Fermi-LAT data. The more sensitive HAWC data, in the energy range 0.5 TeV to 100 TeV, has been reported in Ref. [33] and the corresponding 95% C.L. upper limits in gamma-ray flux is displayed in Fig. 1. The measurements of Fermi-LAT and HAWC are in the right ball park to constraint the photon signals from captured DM as can be seen from Fig. 1.

Gamma ray flux may originate from hadronic interactions of cosmic ray particles in the solar atmosphere [47, 48]. In addition, processes such as Inverse Compton scattering of cosmic-ray electrons with solar photons [49–51] and particle acceleration during severe solar events [52] can produce gamma ray flux indistinguishable to the one investigated here. We keep the exclusion limits modest by assuming that the entire Fermi-LAT and HAWC observations are based on the photon flux from captured DM annihilation, neglecting the aforementioned backgrounds. Our limits will be stronger than the ones stated here if we incorporate all other processes as a background in the observed data. In Fig. 2, the excluded regions of DM-electron scattering cross-section from the Fermi-LAT and HAWC measurements, assuming 100% branching ratio to $\mu\bar{\mu}$ ($\gamma\gamma$) is represented by the blue (red) line and the region above it. The solid and dashed blue (red) contours represent the sensitivity arising from Fermi-LAT and HAWC observations respectively for $\mu\bar{\mu}$ ($\gamma\gamma$) final states. The yellow shaded region depicts the breakdown of equilibrium assumption where for typical WIMP-like annihilation cross-section the captured DM do not reach equilibrium within the solar age [53]. Limits within this region get considerably relaxed. For mediator decay to $\mu\bar{\mu}$, the exclusion limits can reach up to $O(10^{-43} - 10^{-40})$ cm$^2$ which keeps the capture in equilibrium with the annihilation within our parameter space of interest. Strikingly, for the considered scenario the present solar bounds on the DM-electron couplings from the Fermi-LAT and the HAWC pushes the excluded regions to the limit permitted by the equilibrium floor, as can be seen in Fig. 2. The limit obtained by probing neutrino signal of captured DM in Sun is shown for reference [26]. For XENON1T, we obtain the limits by considering S2-only analysis utilizing
Figure 2: Excluded regions of DM-electron scattering cross-section obtained from Fermi-LAT (HAWC) measurements have been shown for two different decay channels: $\gamma\gamma$ with red solid (dashed) line and above and $\mu\bar{\mu}$ with blue solid (dashed) line and above. We have also plotted the constraints obtained by looking at the direct annihilation of captured solar DM in Super-Kamiokande with black dashed line [26] as well as XENON1T bound with black solid line [34, 46]. The region where the equilibrium assumption does not hold for the typical solar age is represented with the yellow shading.

the obscura code [34, 46]. Note that our limits mildly depend on the mediator mass which is set at 5 GeV. The bounds obtained from this analysis, though model dependent, provide the most stringent bounds on the DM-electron scattering cross-section in the considered region of DM parameter space improving the existing bounds by a factor of $\sim 10^4 - 10^6$.

5 Conclusions

Sun, being our host star, is an excellent celestial laboratory to probe non-gravitational interactions of DM. The infalling DM can scatter off electrons inside the Sun and be captured within the solar interior. The annihilation of these captured DM through long-lived mediators can produce considerable gamma-ray flux that can be observed in terrestrial detectors. In this work, we have explored the possibility of searching for the annihilation signatures of electrophilic DM captured inside the Sun utilizing the Fermi-LAT and the HAWC data. We obtain conservative limits by comparing the gamma-ray flux from captured DM annihilating through long-lived mediators with the solar disk measurements of the gamma ray at the Fermi-LAT and the HAWC. We find that in our parameter space of interest, the limits are orders of magnitude stronger than the existing bounds. Depending on the mediator decay mode, the current sensitivity of the observational data approaches the Sun’s equilibrium floor, effectively covering the parameter space that can be explored within this framework.

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