Is a scaling factor required to obtain closure between measured and modelled atmospheric O$_4$ absorptions? An assessment of uncertainties of measurements and radiative transfer simulations for 2 selected days during the MAD-CAT campaign

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Abstract. In this study the consistency between MAX-DOAS measurements and radiative transfer simulations of the atmospheric O$_4$ absorption is investigated on 2 mainly cloud-free days during the MAD-CAT campaign in Mainz, Germany, in summer 2013. In recent years several studies indicated that measurements and radiative transfer simulations of the atmospheric O$_4$ absorption can only be brought into agreement if a so-called scaling factor ($<1$) is applied to the measured O$_4$ absorption. However, many studies, including those based on direct sunlight measurements, came to the opposite conclusion, that there is no need for a scaling factor. Up to now, there is no broad consensus for an explanation of the observed discrepancies between measurements and simulations. Previous studies inferred the need for a scaling factor from the comparison of the aerosol optical depths derived from MAX-DOAS O$_4$ measurements with that derived from coincident sun photometer measurements. In this study a different approach is chosen: the measured O$_4$ absorption at 360 nm is directly compared to the O$_4$ absorption obtained from radiative transfer simulations. The atmospheric conditions used as input for the radiative transfer simulations were taken from independent data sets, in particular from sun photometer and ceilometer measurements at the measurement site. This study has three main goals: first all relevant error sources of the spectral analysis, the radiative transfer simulations and the extraction of the input parameters used for the radiative transfer simulations are quantified. One important result obtained from the analysis of synthetic spectra is that the O$_4$ absorptions derived from the spectral analysis agree within 1% with the corresponding radiative transfer simula-
tions at 360 nm. Based on the results from sensitivity studies, recommendations for optimised settings for the spectral analysis and radiative transfer simulations are given. Second, the measured and simulated results are compared for 2 selected cloud-free days with similar aerosol optical depths but very different aerosol properties. On 18 June, measurements and simulations agree within their (rather large) uncertainties (the ratio of simulated and measured \( \text{O}_4 \) absorptions is found to be \( 1.01 \pm 0.16 \)). In contrast, on 8 July measurements and simulations significantly disagree: for the middle period of that day the ratio of simulated and measured \( \text{O}_4 \) absorptions is found to be \( 0.82 \pm 0.10 \), which differs significantly from unity. Thus, for that day a scaling factor is needed to bring measurements and simulations into agreement. Third, recommendations for further intercomparison exercises are derived. One important recommendation for future studies is that aerosol profile data should be measured at the same wavelengths as the MAX-DOAS measurements. Also, the altitude range without profile information close to the ground should be minimised and detailed information on the aerosol optical and/or microphysical properties should be collected and used.

The results for both days are inconsistent, and no explanation for a \( \text{O}_4 \) scaling factor could be derived in this study. Thus, similar but more extended future studies should be performed, including more measurement days and more instruments. Also, additional wavelengths should be included.

1 Introduction

Observations of the atmospheric absorption of the oxygen collision complex \((\text{O}_2)_2\) (in the following referred to as \( \text{O}_4 \); see Greenblatt et al., 1990) are often used to derive information about atmospheric light paths from remote-sensing measurements of scattered sunlight (for example made from ground, satellite, balloon or airplane). Since atmospheric radiative transport is strongly influenced by scattering on aerosol and cloud particles, information on the presence and properties of clouds and aerosols can be derived from \( \text{O}_4 \) absorption measurements.

Early studies based on \( \text{O}_4 \) measurements focussed on the effect of clouds (e.g. Erle et al., 1995; Wagner et al., 1998, 2014; Winterrath et al., 1999; Acarreta et al., 2004; Sneep et al., 2008; Heue et al., 2014; Gielen et al., 2014), which is usually stronger than that of aerosols. Later aerosol properties were also derived from \( \text{O}_4 \) measurements, in particular from (multi-axis) MAX-DOAS measurements (e.g. Hönninger et al., 2004; Wagner et al., 2004, 2010; Wittrock et al., 2004; Frieß et al., 2006, 2016; Prados-Roman et al., 2011; Irie et al., 2008; Clémer et al., 2010, and references therein). For the retrieval of aerosol profiles forward model simulations for various assumed aerosol profiles are usually compared to measured \( \text{O}_4 \) slant column densities (SCDs, the integrated \( \text{O}_4 \) concentration along the atmospheric light path). The aerosol profile associated with the best fit between the forward model and measurement results is considered to be the most probable atmospheric aerosol profile (for more details, see e.g. Frieß et al., 2006). Note that in some cases no unique solution might exist if different atmospheric aerosol profiles lead to the same \( \text{O}_4 \) absorptions. MAX-DOAS aerosol retrievals are typically restricted to altitudes below about 4 km; see Frieß et al. (2006).

About 10 years ago, Wagner et al. (2009) suggested applying a scaling factor (SF \(< 1\)) to the \( \text{O}_4 \) SCDs derived from MAX-DOAS measurements at 360 nm in Milan in order to achieve agreement with forward model simulations. They found that on a day with low aerosol load the measured \( \text{O}_4 \) SCDs were larger than the model results, even if no aerosols were included in the model simulations. If, however, the measured \( \text{O}_4 \) SCDs were scaled by an SF of 0.81, good agreement with the forward model simulations (and nearby AERONET measurements) was achieved. Similar findings were then reported by Clémer et al. (2010), who suggested an SF of 0.8 for MAX-DOAS measurements in Beijing. Interestingly, they applied this SF to four different \( \text{O}_4 \) absorption bands (360, 477, 577 and 630 nm).

While with the application of an SF the consistency between forward model and measurements was substantially improved, neither study could provide an explanation for the physical mechanism behind such an SF. In the following years several research groups applied an SF in their MAX-DOAS aerosol profile retrievals. However, a similarly large fraction of studies (including direct sun measurements and aircraft measurements; see Spinei et al., 2015) did not find it necessary to apply an SF to bring measurements and forward model simulations into agreement. An overview of the application of an SF to various MAX-DOAS publications after 2010 is provided in Table 1. Up to now, there is no community consensus on whether or not an SF is needed for measured \( \text{O}_4 \) dSCDs. This is a rather unfortunate situation, because this ambiguity directly affects the aerosol results derived from MAX-DOAS measurements and thus the general confidence in the method.

So far, most of the studies deduced the need for an SF in a rather indirect way: aerosol extinction profiles derived from MAX-DOAS measurements using different SF are usually compared to independent data sets (mostly aerosol optical depth, AOD, from sun photometer observations) and the SF leading to the best agreement is selected. In many cases SF between 0.75 and 0.9 were derived.

In this study, we follow a different approach: similarly to Ortega et al. (2016) we directly compare the measured \( \text{O}_4 \) SCDs with the corresponding SCDs derived with a forward model (consisting of a radiative transfer model and assumptions of the state of the atmosphere). For this comparison, atmospheric conditions which are well characterised by independent measurements are chosen. In particular, such a
Table 1. Overview of studies which did not apply a scaling factor (upper part) or did apply a scaling factor (lower part) to the measured O$_4$ dSCDs. Besides the initial studies proposing a scaling factor (Wagner et al., 2009; Clémer et al., 2010), only studies after 2010 are listed.

| Reference                        | Measurement type | Location and period                      | O$_4$ band (nm) | Scaling factor |
|----------------------------------|------------------|------------------------------------------|-----------------|----------------|
| Studies which did not apply a scaling factor$^a$ |                   |                                           |                 |                |
| Thalmann and Volkamer (2010)     | CE-DOAS          | Laboratory                               | 477             | 1              |
| Frieß et al. (2011)              | MAX-DOAS         | Barrow, Alaska (Feb–Apr 2009)            | 360             | 1              |
| Peters et al. (2012)             | MAX-DOAS         | Western Pacific Ocean (Oct 2009)         | 360, 477        | 1              |
| Spinei et al. (2015)             | Direct sun DOAS  | JPL, USA (Jul 2007)                      |                 |                |
|                                 |                  | Pullman, USA (Sep–Nov 2007, Jul–Nov 2011)|                 |                |
|                                 |                  | Fairbanks, USA (Mar–Apr 2011)            |                 |                |
|                                 |                  | Huntsville, USA (Aug 2008)               | 360, 477        | 1              |
|                                 |                  | Richland, USA (Apr–Jun 2008)             |                 |                |
|                                 |                  | Greenbelt, USA (May 2007, 2012–2014)     |                 |                |
|                                 |                  | Cabauw, the Netherlands (Jun–Jul 2009)   |                 |                |
| Spinei et al. (2015)             | Airborne DOAS    | Subtropical Pacific Ocean (Jan 2012)     | 360, 477        | 1              |
| Ortega et al. (2016)             | MAX-DOAS         | Cape Cod, USA (Jul 2012)                 | 360, 477        | 1              |
| Schreier et al. (2016)           | MAX-DOAS         | Zugspitze, Germany (Apr–Jul 2003)       | 360             | 1              |
| Seyler et al. (2017)             | MAX-DOAS         | German Bight (2013–2016)                 | 360             | 1              |
| Wang et al. (2017b, c)           | MAX-DOAS         | Wuxi, China (2011–2014)                  | 360             | 1              |
| Gielen et al. (2017)             | MAX-DOAS         | Bujumbura, Burundi (2013–2015)           | 360             | 1              |
| Franco et al. (2015)             | MAX-DOAS         | Jungfraujoch (2010–2012)                 | 360             | 1              |
| Studies which did apply a scaling factor |                   |                                           |                 |                |
| Wagner et al. (2009)             | MAX-DOAS         | Milano, Italy Sep 2013 (FORMAT II)       | 360             | 0.81           |
| Clémer et al. (2010)             | MAX-DOAS         | Beijing, China Jul 2008–Apr 2009         | 360, 577, 630   | 0.80           |
| Irie et al. (2011)               | MAX-DOAS         | Cabauw, the Netherlands Jul–Jun 2009 (CINDI-I) | 360, 477   | 0.75 ± 0.1   |
| Merlaud et al. (2011)            | Airborne DOAS    | Arctic Apr 2008 POLARCAT                 | 360             | 0.89           |
| Vlemmix et al. (2011)            | MAX-DOAS         | Cabauw, the Netherlands Jul–Oct 2009 (CINDI-I) | 360 (MPIC) | 0.83           |
| Zieger et al. (2011)             | Overview of MAX-DOAS | Cabauw, the Netherlands Jul–Oct 2009 (CINDI-I) | 360 (MPIC) | 0.83           |
| Wang et al. (2014)               | MAX-DOAS         | Xianghe, China (2010–2013)               | 360             | 0.8            |
| Kanaya et al. (2014)             | MAX-DOAS         | Cape Hedo, Japan (2007–2012)             | 477             | 0.8            |
|                                 |                  | Fukue, Japan (2008–2012)                 | 477             | 0.8            |
|                                 |                  | Yokosuda, Japan (2007–2012)              | 477             | 0.8            |
|                                 |                  | Gwangju, Korea (2008–2012)               | 477             | 0.8            |
|                                 |                  | Hefei, China (2008–2012)                 | 477             | 0.8            |
|                                 |                  | Zvenigorod, Russia (2009–2012)           | 477             | 0.8            |
| Hendrick et al. (2014)           | MAX-DOAS         | Beijing, China (2008–2009)               | 360             | 0.8            |
|                                 |                  | Xianghe, China (2010–2012)               |                 |                |
| Vlemmix et al. (2015)            | MAX-DOAS         | Beijing, China (2008–2009)               | 360, 477        | 0.8            |
|                                 |                  | Xianghe, China (2010–2012)               |                 |                |
| Irie et al. (2015)               | MAX-DOAS         | Tsukuba, Japan (Oct 2010)                | 477             | elevation-dependent scaling factor$^b$ |
| Wang et al. (2016)               | MAX-DOAS         | Madrid, Spain (Mar–Sep 2015)             | 360             | 0.83           |
| Frieß et al. (2016)              | MAX-DOAS         | Cabauw, the Netherlands Jul–Jul 2009 (CINDI-I) | 477 (AOIFM) | 0.8           |
|                                 |                  |                                          | 477 (BIRA)      | 0.8            |
|                                 |                  |                                          | 477 (IUPHD)     | 1              |
|                                 |                  |                                          | 477 (JAMSTEC)   | 0.8$^c$        |
|                                 |                  |                                          | 360 (MPIC)      | 0.77           |

$^a$ The authors of part of these studies were probably not aware that a scaling factor was applied by other groups.
$^b$ SF = $1/(1 + EA/60)$.
$^c$ SF is varied during profile inversion.
procedure allows the influence of the uncertainties of the individual processing steps to be quantified.

One peculiarity of this comparison is that the measured O\textsubscript{4} SCDs are first converted into their corresponding air mass factors (AMFs), which are defined as the ratio of the SCD and the vertical column density (VCD, the vertically integrated concentration) (Solomon et al., 1987).

\[
\text{AMF} = \frac{\text{SCD}}{\text{VCD}}
\]  
(1)

The “measured” O\textsubscript{4} AMF is then compared to the corresponding AMF derived from radiative transfer simulations for the atmospheric conditions during the measurements:

\[
\text{AMF}_{\text{measured}} \neq \text{AMF}_{\text{simulated}}.
\]  
(2)

The conversion of the measured O\textsubscript{4} SCDs into AMFs is carried out to ensure a simple and direct comparison between measurements and forward model simulations. Here it should be noted that in addition to the AMFs so-called differential AMFs (dAMFs) will be compared in this study. The dAMFs represent the difference between AMFs for measurements at non-zenith elevation angles \(\alpha\) and at 90\(^{\circ}\) for the same elevation sequence:

\[
d\text{AMF}_\alpha = \text{AMF}_\alpha - \text{AMF}_{90^\circ}.
\]  
(3)

Note that in this paper the following notations are used:

- AMF is the air mass factor.
- dAMF is the differential air mass factor.
- (d)AMF is the air mass factor and/or differential air mass factor (similar notations are used for the (d)SCDs).

For the comparison between measured and simulated O\textsubscript{4} (d)AMFs, 2 mostly cloud-free days (18 June and 8 July 2013) during the Multi Axis DOAS Comparison campaign for Aerosols and Trace gases (MAD-CAT) campaign are chosen (http://joseba.mpch-mainz.mpg.de/mad_cat.htm, last access: 29 April 2019). As discussed in more detail in Sect. 4.2.2, based on the ceilometer and sun photometer measurements, three periods on each of the 2 selected days are selected, during which the variation of the aerosol profiles was relatively small (see Table 2). In addition to the aerosol profiles, other atmospheric properties are averaged during these periods before they are used as input for the radiative transfer simulations.

The comparison is carried out for the O\textsubscript{4} absorption band at 360 nm, which is the strongest O\textsubscript{4} absorption band in the UV. In principle other O\textsubscript{4} absorption bands (e.g. in the visible spectral range) could also be chosen, but these bands are not covered by the wavelength range of the MPIC instrument. Thus, they are not part of this study.

The comparison between measurements and simulations is performed in three different steps: first, for selected periods in the middle of each day, the ratios between measured and simulated O\textsubscript{4} (d)AMFs are calculated for “standard settings” of the spectral retrieval and radiative transfer simulations (for details see below). In a second step, the uncertainties of the measurements and simulations are investigated. In the final step, it is investigated whether the ratio of measured and simulated O\textsubscript{4} (d)AMFs agree with unity when taking into account these uncertainties.

Deviations between the forward model and measurements can have different causes. In the following an overview of these error sources and the way they are investigated in this study are given:

1. Calculation of O\textsubscript{4} profiles and O\textsubscript{4} VCDs (Eq. 1).

Profiles and VCDs of O\textsubscript{4} are derived from pressure and temperature profiles. The uncertainties of the pressure and temperature profiles are quantified by sensitivity studies and by the comparison of the extraction results derived from different groups or persons (see Table 3).

2. Calculation of O\textsubscript{4} (d)AMFs from radiative transfer simulations.

Besides differences between the different radiative transfer codes, the dominating sources of uncertainty are those related to the input parameters. They are investigated by sensitivity studies and by the comparison of extracted input data by different groups or persons. Also, the effects of operating different radiative transfer models by different groups are investigated.

3. Analysis of the O\textsubscript{4} (d)AMFs from MAX-DOAS measurements.

Uncertainties in the spectral analysis results are caused by errors and imperfections in the measurements and instruments, the dependence of the analysis results on the specific fit settings and the uncertainties of the O\textsubscript{4} cross sections including their temperature dependence. They are investigated by systematic variation of the DOAS fit settings (for measured and synthetic spectra) and by comparison of analysis results obtained from different groups and/or instruments.

The paper is organised as follows: in Sect. 2, information on the selected days during the MAD-CAT campaign, on the MAX-DOAS measurements and on the data sets from independent measurements is provided. Section 3 presents the initial comparison results for the selected days using standard settings. In Sect. 4 the uncertainties associated with each of the various processing steps of the spectral analysis and the forward model simulations are quantified by being compared to the results for the standard settings. Section 5 presents a summary and conclusions.
Table 2. Periods on both selected days, which are used for the comparisons.

| Day         | First period       | Second period      | Third period        |
|-------------|--------------------|--------------------|---------------------|
| 18 June 2013| 08:00–11:00 UTC    | 11:00–14:00 UTC    | 14:00–19:00 UTC     |
| 8 July 2013 | 04:00–07:00 UTC    | 07:00–11:00 UTC    | 11:00–19:00 UTC     |

Table 3. Participation of the different groups in the different analysis steps.

| Abbreviation | Institution                                             | Determination of the $O_4$ profile and VCD | Extraction of aerosol profiles | Radiative transfer simulations | Spectral analysis |
|--------------|---------------------------------------------------------|--------------------------------------------|-------------------------------|-------------------------------|------------------|
| BIRA         | BIRA/IASB, Brussels, Belgium                            |                                            |                               |                               |                  |
| CMA          | Meteorological Observation Center, Beijing, China       | •                                          |                               |                               |                  |
| CSIC         | Department of Atmospheric Chemistry and Climate, Institute of Physical Chemistry Rocasolano (CSIC), Spain | •                                          |                               |                               |                  |
| INTA         | Instituto Nacional de Tecnica Aeronautica, Spain        |                                            |                               | •                              | •                |
| IUP-B        | University of Bremen, Germany                           |                                            |                               | •                              | •                |
| IUP-HD       | University of Heidelberg, Germany                       |                                            |                               | •                              | •                |
| LMU          | Ludwig-Maximilians-Universitat Munchen, Germany         | •                                          |                               |                               | •                |
| MPIC         | MPI for Chemistry, Mainz, Germany                       | •                                          |                               | •                              | •                |

2 MAD-CAT campaign, MAX-DOAS instruments and other data sets used in this study

The Multi Axis DOAS Comparison campaign for Aerosols and Trace gases (MAD-CAT) (http://joseba.mpch-mainz.mpg.de/mad_cat.htm) took place in June and July 2013 on the roof of the Max Planck Institute for Chemistry in Mainz, Germany. The main aim of the campaign was to compare MAX-DOAS retrieval results of several atmospheric trace gases like NO$_2$, HCHO, HONO and CHOCHO as well as aerosols. The measurement location was at 150 m above sea level at the western edge of the city of Mainz.

2.1 MAX-DOAS instruments

During the MAD-CAT campaign, 11 MAX-DOAS instruments were operated by different groups; an overview can be found at the website http://joseba.mpch-mainz.mpg.de/equipment.htm (last access: 29 April 2019). The main viewing direction of the MAX-DOAS instruments was towards north-west (51° with respect to north). Measurements at this viewing direction were the main focus of this study, but a few comparisons using the standard settings (see Sect. 3) were also carried out for three other azimuth angles (141, 231, 321°; see Fig. A2I in Appendix A1). Each elevation sequence contains the following elevation angles: 1, 2, 3, 4, 5, 6, 8, 10, 15, 30 and 90°. In this study, in addition to the MPIC instrument, spectra from three other MAX-DOAS instruments were also analysed. The instrument details are given in Table 4. The spectra of the MPIC instrument are available at the website http://joseba.mpch-mainz.mpg.de/e_doc_zip.htm (last access: 29 April 2019).

2.2 Additional data sets

In order to constrain the radiative transfer simulations, independent measurements and data sets were used. In particular, information on atmospheric pressure, temperature and relative humidity, as well as aerosol properties, is used. In addition to local in situ measurements from air quality monitoring stations and remote-sensing measurements by a ceilometer and a sun photometer, ECMWF reanalysis data were used. An overview of these data sets is given in Table 5. The data sets used in this study are available at the websites http://joseba.mpch-mainz.mpg.de/a_doc_zip.htm (last access: 29 April 2019) and http://joseba.mpch-mainz.mpg.de/e_doc_zip.htm (last access: 29 April 2019).

2.3 RTM simulations

Several radiative transfer models are used to calculate $O_4$ (d)AMFs for the selected days. As input, vertical profiles of...
Table 4. Overview of properties of MAX-DOAS instruments participating in this study.

| Institute/instrument type | Spectral range (nm) | Spectral resolution (FWHM, nm) | Spectral range per detector pixel (nm) | Detector type/temperature | Integration time of individual spectra (s) | Reference |
|---------------------------|---------------------|-------------------------------|----------------------------------------|---------------------------|------------------------------------------|-----------|
| BIRA/2-D scanning MAX-DOAS| 300–386             | 0.49                          | 0.04                                   | 2-D back-illuminated CCD, 2048 × 512 pixels/−40°C | 60                        | Clémer et al. (2010) |
| IUP Bremen/2-D scanning MAX-DOAS| 308–376           | 0.43                          | 0.05                                   | 2-D back-illuminated CCD, 1340 × 400 pixels/−35°C | 20                        | Peters et al. (2012) |
| IUP-Heidelberg/1-D scanning MAX-DOAS| 294–459           | 0.59                          | 0.09                                   | AvaSpec-ULS 2048 pixels back-thinned Hamamatsu CCD S11071-1106/20°C | 60                        | Lampel et al. (2015) |
| MPIC/4-azimuth MAX-DOAS   | 320–457             | 0.67                          | 0.14                                   | 2-D back-illuminated CCD, 1024 × 255 Pixels/−30°C | 10 s                      | Krautwurst (2010) |

Table 5. Independent data sets used to constrain the atmospheric properties on both selected days.

| Measurement or data set | Measured quantities | Derived quantities | Temporal or spatial resolution | Source |
|-------------------------|---------------------|--------------------|-------------------------------|--------|
| Ceilometer              | Attenuated backscatter profiles a at 1064 nm | Aerosol extinction profiles at 360 nm | 30 s/15 m | Wiegner and Geiß (2012) |
| AERONET sun photometer  | Solar irradiances, sky radiances | Aerosol optical depth, single-scattering albedo, phase function | Typical integration time: 2 to 15 min | Holben et al. (2001), https://aeronet.gsfc.nasa.gov/ (last access: 29 April 2019) |
| Surface measurements air quality stations in Mainz Mombach | Temperature, pressure, relative humidity | | 1 h | http://www.luft-rlp.de (last access: 29 April 2019) |
| Surface measurements air quality stations in Mainz and Wiesbaden | PM2.5 | | 1 h (Mainz stations) | http://www.luft-rlp.de |
| | PM10 | | 30 min (Wiesbaden stations)c | https://www.hlnug.de/themen/luft/luftmessnetz.html |
| ECMWF ERA-Interim reanalysis | Temperature, pressure, relative humidity | | Average over the area 49.41–50.53°N, 7.88–9.00°E, every 6 h | Dee et al. (2011) |

a There is no useful signal below 180 m due to limited overlap.

b Here 15 min averages are used.

c Stations in Mainz are Parcusstrasse, Zitadelle and Mombach. Stations in Wiesbaden are Schierstein, Ringkirche and Süd.

temperature, pressure, relative humidity and aerosol extinction extracted from the independent data sets (see Sects. 2.2 and 4) were used. The vertical resolution is high in the lowest layers and decreases with increasing altitude (see Table A1 in Appendix A1). The upper boundary of the vertical grid is set to 1000 km. The lower boundary of the model grid represents the surface elevation of the instrument (150 m above sea level). For the standard run, a surface albedo of 5% is assumed and the aerosol optical properties are described by a Henyey–Greenstein phase function with an asymmetry parameter of 0.68 and a single-scattering albedo of 0.95. Both values represent typical urban aerosols (see e.g. Dubovik et al., 2002). Ozone absorption was not considered, because it is very small at 360 nm. The MAD-CAT campaign took place around the summer solstice. Thus, the same dependence of the solar zenith angle (SZA) and relative azimuth angle (RAZI) on time is used for both days (see Table A2 in the Appendix A1). The input data used for the radiative transfer simulations are available at the website http://joseba.mpch-mainz.mpg.de/d_doc_zip.htm (last access: 29 April 2019). In the following subsections
the different radiative transfer models used in this study are described.

2.3.1 McArtim

The full spherical Monte Carlo radiative transfer model, McArtim (Deutschmann et al., 2011), explicitly simulates individual photon trajectories including the photon interactions with molecules, aerosol particles and the surface. In this study, two versions of McArtim are used: version 1 and version 3. Version 1 is a 1-D scalar model. Version 3 can also be run in 3-D and vector modes. In version 1 rotational Raman scattering (RRS) is partly taken into account: the RRS cross section and phase function are explicitly considered for the determination of the photon paths, but the wavelength redistribution during the RRS events is not considered. In version 3 RRS can be fully taken into account. If operated in the same mode (1-D scalar), both models show excellent agreement.

2.3.2 LIDORT

In this study the LIDORT version 3.3 was used. The Linearized Discrete Ordinate Radiative Transfer (LIDORT) forward model (Spurr et al., 2001, 2008) is based on the discrete ordinate method to solve the radiative transfer equation (e.g. Chandrasekhar, 1960, 1989; Stamnes et al., 1988). This model considers a pseudo-spherical multilayered atmosphere including several anisotropic scatters. The formulation implemented corrects for the atmosphere curvature in the solar and single-scattered beams; however the multiple-scattering term is treated in the plane-parallel approximation. The properties of each of the atmospheric layers are considered homogeneous in the corresponding layer. Using finite differences for the altitude derivatives, this linearised code converts the problem into a linear algebraic system. Through first-order perturbation theory, it is able to provide radiance and radiance derivatives with respect to atmospheric and surface variables (Jacobians) in a single call. LIDORT was used in several studies to derive vertical profiles of aerosols and trace gases from MAX-DOAS (e.g. Clémer et al., 2010; Hendrick et al., 2014; Franco et al., 2015).

2.3.3 SCIATRAN

The RTM SCIATRAN (Rozanov et al., 2014) was used in its full-spherical mode including multiple scattering but without polarisation. In the operation mode used here, SCIATRAN solves the transfer equations using the discrete ordinate method. In this study, SCIATRAN was used by two groups: the IUP Bremen group used v3.8.3 for the O₄ dAMFs simulations (without Raman scattering). The MPIC group used v3.6.11 for the calculation of synthetic spectra (see Sect. 2.4) and for the O₄ dAMFs simulations (including Raman scattering).

2.4 Synthetic spectra

In addition to AMFs and dAMFs, synthetic spectra were simulated. They are analysed in the same way as the measured spectra, which allows the investigation of two important aspects:

1. The derived O₄ dAMFs from the synthetic spectra can be compared to the O₄ dAMFs obtained directly from the radiative simulations at one wavelength (here, 360 nm) using the same settings. In this way the consistency of the spectral analysis results and the radiative transfer simulations is tested.

2. Sensitivity tests can be performed by varying several fit parameters, e.g. the spectral range or the DOAS polynomial, and their effect on the derived O₄ dAMFs can be assessed.

Synthetic spectra are simulated using SCIATRAN while taking into account rotational Raman scattering. The basic simulation settings are the same as for the RTM simulations of the O₄ (d)AMFs described above. In order to minimise the computational effort, for the profiles of temperature, pressure, relative humidity and aerosol extinction the input data for only two periods (18 June on 11:00–14:00 UTC, 8 July on 07:00–11:00; see Table 2) are used for the whole day. Thus, “perfect” agreement with the measurements can only be expected for the two selected periods. Aerosol optical properties (phase function and single-scattering albedo) are taken from AERONET measurements of the 2 selected days. Although the wavelength dependencies of both quantities (and also for the aerosol extinction) are considered, it should be noted that the associated uncertainties are probably rather large, since the optical properties in the UV had to be extrapolated from measurements in the visible spectral range.

Spectra were simulated at a spectral resolution of 0.01 nm and convolved with a Gaussian slit function of 0.6 nm full width at half maximum (FWHM), which is similar to those of the measurements. For the generation of the spectra a high-resolution solar spectrum (Chance and Kurucz, 2010) and the trace gas absorptions of O₃, NO₂, HCHO and O₄ are considered (see Table A3 in Appendix A1). The assumed tropospheric profiles of NO₂ and HCHO are similar to those retrieved from the MAX-DOAS observations during the selected periods. Time series of the tropospheric VCDs of NO₂ and HCHO for the 2 selected days are shown in Fig. A1 in Appendix A1.

Two sets of synthetic spectra were simulated, one taking into account the temperature dependence of the O₃ cross section and the other not. For the case that not consider the temperature dependence, the O₄ cross section for 293 K is used. In addition to spectra without noise, spectra with noise (sigma of the noise is assumed as 7.5 × 10⁻⁴ times the intensity) were simulated. The synthetic spectra are available at the website http://joseba.mpch-mainz.mpg.de/f_doc_zip.htm (last access: 29 April 2019).
3 Strategies used in this study and comparison results for the standard settings

3.1 Selection of days

For the comparison of measured and simulated O$_4$ dAMFs, 2 mostly cloud-free days during the MAD-CAT campaign (18 June and 8 July 2013) were selected. On both days the AOD measured by the AERONET sun photometer at 360 nm was between 0.25 and 0.4 (see Fig. 1). In spite of the similar AODs, very different aerosol properties at the surface were found on the 2 selected days: on 18 June much higher concentrations of large aerosol particles (PM$_{2.5}$ and PM$_{10}$) are found. These differences are also represented by the large differences in the Ångström exponent for long wavelengths (440–870 nm) on both days. Also, the aerosol height profiles are different: on 8 July rather homogenous profiles with a layer height of about 2 km occur. On 18 June the aerosol profiles reach higher altitudes, but the highest extinction is found close to the surface. Also, the temporal variability of the aerosol properties, especially the near-surface concentrations, is much larger on 18 June.

3.2 Different levels of comparisons

The comparison between the forward model and MAX-DOAS measurements is performed at different depths for different subsets of the measurements:

1. A quantitative comparison of O$_4$ AMFs and O$_4$ dAMFs is performed for 3° elevation angle at the standard viewing direction (51° with respect to north) for the middle period of each selected day. During these periods the uncertainties of the measurement and the radiative transfer simulations are smallest because around noon the measured intensities are high and the variation of the SZA is small. During the selected periods, the variation of the ceilometer profiles is also relatively small. These comparisons thus constitute the core of the comparison exercise and all sensitivity studies are performed for these two periods. The elevation angle of 3° is selected because for such a low-elevation angle the atmospheric light paths and thus the O$_4$ absorption is rather large. Moreover, as can be seen in Fig. 2, the O$_4$ (d)AMFs for 3° are very similar to those for 1 and 6°, especially on 8 July 2013. Sensitivity studies showed that a wrong elevation angle calibration (±0.5°) led to only small changes (<1 %) in the O$_4$ (d)AMFs. Changes in the field of view between 0.2 and 1.1° led to even smaller differences. These findings indicate that possible uncertainties of the calibration of the elevation angles of the instruments can be neglected. Here it is interesting to note that on 18 June even slightly lower O$_4$ (d)AMFs are found for the low-elevation angles. This is in agreement with the finding of high aerosol extinction in a shallow layer above the surface (see Fig. 1). The azimuth angle of 51° was chosen, because it was the standard viewing direction during the MAD-CAT campaign and measurements for this direction are available from different instruments.

2. The quantitative comparison for 3° elevation and an azimuth of 51° is also extended to the periods prior to and after the middle periods of the selected days. However, to minimise the computational efforts, some sensitivity studies are not carried out for the first and last periods.

3. The comparison is extended to more elevation angles (1, 3, 6, 10, 15, 30, 90°) and azimuth angles (51, 141, 231, 321°). For this comparison only the standard settings for the DOAS analysis and the radiative transfer simulations are applied (see Tables 6 and 7). The comparison results for the MPIC MAX-DOAS measurements are shown in Appendix A2. The purpose of this comparison is to check whether for other viewing angles similar results are found as for 3° elevation at 51° azimuth direction.

3.3 Quantitative comparison for 3° elevation in standard azimuth direction

Figure 3 presents a comparison of the measured and simulated O$_4$ (d)AMFs for 3° elevation and 51° azimuth on both days. For the spectral analysis and the radiative transfer simulations the respective standard settings (see Tables 6 and 7) were used. On 8 July the simulated O$_4$ (d)AMFs systematically underestimate the measured O$_4$ (d)AMFs by up to 40 %. Similar results are obtained for other elevation and azimuth angles (see Appendix A2), with the differences becoming smaller towards higher elevation angles. In contrast, no systematic underestimation is observed for most of 18 June. For some periods of that day the simulated O$_4$ (d)AMFs are even larger than the measured O$_4$ (d)AMFs. However, here it should be noted that the aerosol extinction profile of the standard settings (using linear extrapolation below 180 m where no ceilometer data are available) probably underestimates the aerosol extinction close to the surface. If instead a modified aerosol profile with strongly increased aerosol extinction below 180 m and the maximum AOD during that period is used (see Fig. A31 in Appendix A5), the corresponding (d)AMFs fall below the measured O$_4$ (d)AMFs (green curves in Fig. A4 in Appendix A2). More details on the extraction of the aerosol extinction profiles are given in Sect. 4.2.2 and Appendix A5).

The average ratio of simulated to measured (d)AMFs (for the standard settings) during the middle period on each day are given in Table 8. For 18 June they are close to unity, but for 8 July they are much lower (0.83 for the AMF and 0.69 for the dAMF).
Figure 1. Various aerosol properties on the 2 selected days (left: 18 June 2013; right: 8 July 2013). (a) Aerosol backscatter profiles from ceilometer measurements. (b) AOD at 340, 360 and 380 nm (360 values are interpolated from 340 and 380 nm) from AERONET sun photometer measurements. (c) Ångström exponents for two wavelength pairs (340–440 and 440–870 nm) from AERONET sun photometer measurements. (d) Surface in situ measurements of PM$_{2.5}$ and PM$_{10}$ measured at different air quality monitoring stations in Mainz and the nearby city of Wiesbaden.

Table 6. Standard settings for the radiative transfer simulations.

| Parameter                        | Standard setting                                      |
|----------------------------------|-------------------------------------------------------|
| Temperature and pressure profile | MPIC extraction                                      |
| O$_4$ profile                    | MPIC extraction                                      |
| Surface albedo                   | 5 %                                                   |
| Aerosol single-scattering albedo | 0.95                                                  |
| Aerosol phase function           | HG model with asymmetry parameter of 0.68             |
| Aerosol extinction profile       | MPIC extraction with linear interpolation < 180 m     |
| Polarisation                     | Not considered                                        |
| Raman scattering                 | Partly considered for synthetic spectra               |
Figure 2. $O_4$ AMFs (upper lines) and dAMFs (lower lines) for 1, 3 and $6^\circ$ elevation angles derived from the MPIC MAX-DOAS measurements on the 2 selected days. Interestingly, on 18 June the lowest values are in general found for the lowest elevation angles, which is an indication for the high aerosol load close to the surface. The y axis on the right shows the corresponding $O_4$ (d)SCDs for $O_4$ VCDs of $1.23 \times 10^{43}$ molecules$^2$ cm$^{-5}$ and $1.28 \times 10^{43}$ molecules$^2$ cm$^{-5}$ for 18 June and 8 July, respectively (see Sect. 4.1.2).

Figure 3. (a) Comparison of $O_4$ (d)AMFs from MAX-DOAS measurements and forward model simulations for the 2 selected days. The green rectangle indicates the middle period on each day, which are the focus of the quantitative comparison. The green line on 18 June represents forward model results for a modified aerosol profile (see text). The y axis on the right shows the corresponding $O_4$ (d)SCDs for $O_4$ VCDs of $1.23 \times 10^{43}$ molecules$^2$ cm$^{-5}$ and $1.28 \times 10^{43}$ molecules$^2$ cm$^{-5}$ for 18 June and 8 July, respectively (see Sect. 4.1.2). In (b) and (c) the ratios of the simulated and measured AMFs and dAMFs are shown, respectively. The red line on 18 June represents the ratios for the modified aerosol scenario.
Table 7. Standard settings for the DOAS analysis of $O_4$.

| Parameter                                | Value, remark or reference                                                                 |
|------------------------------------------|-------------------------------------------------------------------------------------------|
| Spectral range                           | 352–387 nm                                                                                 |
| Degree of DOAS polynomial                | 5                                                                                          |
| Degree of intensity offset polynomial    | 2                                                                                          |
| Fraunhofer reference spectrum            | 8 July, 10:05:35, SZA: 32.37°, elevation angle: 90° (this spectrum is used for both days) |
| Wavelength calibration                   | Fit to high-resolution solar spectrum using Gaussian slit function                          |
| Shift/squeeze                            | The measured spectrum is shifted and squeezed against all other spectra                     |
| Ring spectrum 1                          | Normal Ring spectrum calculated from DOASIS                                                 |
| Ring spectrum 2                          | Ring spectrum 1 multiplied by $\lambda^{-4}$                                                |
| $O_3$ cross section                      | 223 K, Bogumil et al. (2003)                                                               |
| NO$_2$ cross section                     | 294 K, Vandaele et al. (1997)                                                              |
| BrO cross section                        | 223 K, Fleischmann et al. (2004)                                                           |
| $O_4$ cross section                      | 293 K, Thalman and Volkamer (2013)                                                         |

Table 8. Average ratios (simulation results divided by measurements) of the $O_4$ (d)AMFs for the middle periods of the selected days.

| Period                  | AMF ratio | dAMF ratio |
|-------------------------|-----------|------------|
| 18 Jun 2013, 11:00–14:00| 0.97      | 0.94       |
| 8 Jul 2013, 07:00–11:00 | 0.83      | 0.69       |

4 Estimation of the uncertainties of the different processing steps

There are three major processing steps, for which the uncertainties are quantified in this section:

1. the determination of the $O_4$ height profiles and corresponding $O_4$ VCDs,
2. the simulation of $O_4$ (d)AMFs by the forward model,
3. the analysis of $O_4$ (d)AMFs from the MAX-DOAS measurements.

4.1 Determination of the vertical $O_4$ profile and the $O_4$ VCD

The $O_4$ VCD is required for conversion of measured (d)SCDs into (d)AMFs (Eq. 1). $O_4$ profiles are also needed for the calculation of $O_4$ (d)AMFs. The accuracy of the calculated $O_4$ height profile and the $O_4$ VCD depends in particular on two aspects:

1. Is profile information on temperature, pressure and (relative) humidity available?
2. What is the accuracy of these data sets?

Additional uncertainties are related to the details of the calculation of the $O_4$ concentration and $O_4$ VCDs from these profiles. Both sources of uncertainties are investigated in the following subsections.

4.1.1 Extraction of vertical profiles of temperature and pressure

The procedure of extracting temperature and pressure profiles depends on the availability of measured profile data or surface measurements. If profile data are available (e.g. from sondes or models) they could be directly used. If only surface measurements are available, vertical profiles of temperature and pressure could be calculated by making assumptions on the lapse rate (here we assume a value of $-0.65$ K/100 m). If no measurements or model data are available, profiles from the US standard atmosphere might be used (United States Committee on Extension to the Standard Atmosphere, 1976). In Appendix A3 the different procedures for the extraction of pressure and temperature profiles are described in detail for the 2 selected days of the MAD-CAT campaign. For these days the optimum choice was to combine the model data and the surface measurements. In that way, the diurnal variation in the boundary layer could be considered. In Fig. 4 temperature and pressure profiles extracted from the combination of in situ measurements and ECMWF data are shown. These profiles probably best match the true atmospheric profiles.

A comparison of temperature profiles extracted by different methods for two selected periods on both days is shown in Fig. 5. For 8 July (right), a rather good agreement is found, but for 18 June (left) the agreement is worse (differences up to 20 K). Of course, the differences between the true and the US standard atmosphere profiles can become even larger, depending on location and season. So the use of a fixed temperature and pressure profile should always be the last choice. In contrast, the simple extrapolation from surface values can be very useful if no profile data are available, because the uncertainties of this method are usually smallest at low altitudes, where the bulk of $O_4$ is located.
is an \(O_4\) scaling factor required?

Figure 4. Extracted temperature (a) and pressure (b) profiles for the three periods on 8 July 2013. Also shown are ECMWF profiles above Mainz for 06:00 and 18:00. To better account for the diurnal variation of the temperatures near the surface, below 1 km the temperature is linearly interpolated between the surface measurements and the ECMWF temperatures at 1 km (for details see text). Note that the altitude is given relative to the height of the measurement site (150 m).

Figure 5. Temperature profiles extracted in different ways for two periods, (a) 18 June, 14:00–19:00 and (b) 8 July, 04:00–07:00. The blue profiles are extracted from in situ measurements and ECMWF profiles as described in the text. The green profiles are extracted from the surface temperatures and assume a constant lapse rate of \(-6.5\) K/km up to 12 km and a constant temperature above. The pink curves represent the temperature profile from the US standard atmosphere.

4.1.2 Calculation of \(O_4\) concentration profiles and \(O_4\) VCDs

From the temperature and pressure profiles the oxygen (\(O_2\)) concentration is calculated. Here, the effect of the atmospheric humidity profiles should also be taken into account (see Appendix A3), because it can have a considerable effect on the near-surface layers (at least for temperatures of about > 20°C). Finally, the square of the oxygen concentration is calculated and used as proxy for the \(O_4\) concentration consistently with assumptions made in the determination of the absorption cross sections (see Greenblatt et al., 1990). The uncertainties of the derived \(O_4\) concentration (and the corresponding \(O_4\) VCD) caused by the uncertainty of the input profiles is estimated by varying the input parameters (for details see Appendix A3).

For both selected days during the MAD-CAT campaign the total uncertainty is estimated to be about 1.5% assuming that the uncertainties of the individual input parameters are independent.

Further uncertainties arise from the procedure of the vertical integration of the \(O_4\) concentration profiles. We tested the effect of using different vertical grids and altitude ranges. It is found that the vertical grid should not be coarser than 100 m (for which a deviation in the \(O_4\) VCD of 0.3% compared to a much finer grid is found). If, for example, a vertical grid with 500 m layers is used, the deviation increases to about 1.3%. The integration should be performed over an altitude range up to 30 km. If lower maximum altitudes are used, the \(O_4\) VCD will be substantially underestimated: deviations of 0.1%, 0.5% and 11% are found if the integration is performed only up to 25, 20 and 10 km, respectively. Here it should be noted that the exact consideration of the altitude of the measurement site is also very important: a deviation of 50 m already leads to a change in the \(O_4\) VCD of 1%. For the MAD-CAT measurements the altitude of the instruments is 150 m ± 20 m.

Finally, the effects of individual extraction and integration procedures are investigated by comparing the results from different groups (see Fig. 6 and Fig. A5 in Appendix A3). Except for some extreme cases, the extracted temperatures typically differ by less than 3 K below 10 km. However, the deviations are typically larger for the profiles extrapolated from the surface values and in particular for the US standard atmosphere (up to > 10 K below 10 km). The variations of the extracted pressure profiles are in general rather small (< 1% below 10 km, except one obvious outlier). However, the deviations in the profiles extrapolated from the surface values, and especially the US standard atmosphere, are much larger (up to > 5% below 10 km). The resulting deviations in the \(O_4\) concentration from the different extractions are typically < 3% below 10 km (and up to > 20% above 10 km for the US standard atmosphere).

In Fig. 7 the \(O_4\) VCDs calculated for the \(O_4\) profiles extracted from the different groups and for the profiles extrapolated from the surface values and the US standard atmosphere are shown. The VCDs for the profiles extracted by the different groups agree within 2.5%. The deviations in the profiles extrapolated from the surface values are only slightly larger (typically within 3%) but show a large variability throughout the day, which is caused by the systematic increase in the surface temperature during the day (with temperature inversions in the morning on the 2 selected days). The deviations of the US standard atmosphere are up to 5% (but can of course
be larger for other seasons and locations; see also Ortega et al. (2016).

Ultimately, the accuracy with which $O_4$ concentrations can be calculated is limited by the assumption that $O_4$ ($O_2$-$O_2$) is pure collision-induced absorption. If the oxygen concentration profile is well known, the uncertainty due to bound $O_4$ is smaller than 0.14 % in the Earth’s atmosphere (Thalman and Volkamer, 2013).

Together with the uncertainties related to the input data sets, the total uncertainty of the $O_4$ VCDs determined for both selected days is estimated at 3 %.

4.2 Uncertainties of the $O_4$ (d)AMFs derived from radiative transfer simulations

The most important uncertainties of the simulated $O_4$ (d)AMFs are related to the uncertainties of the input parameters used for the simulations, in particular the aerosol properties. Further uncertainties are caused by imperfections in the radiative transfer models. These sources of uncertainty are discussed and quantified in the following subsections.

4.2.1 Uncertainties of the $O_4$ (d)AMFs caused by uncertainties of the input parameters

In this section the effect of the uncertainties of various input parameters on the $O_4$ (d)AMFs is investigated. The general procedure is that the input parameters are varied individually and the corresponding changes in the $O_4$ (d)AMFs compared to the standard settings are quantified.

First, the effect of the $O_4$ profile shape is investigated. In contrast to the effect of the (absolute) profile shape on the $O_4$ VCD (Sect. 4.1), here the effect of the relative profile shape on the $O_4$ AMF is investigated. The $O_4$ (d)AMFs simulated for the $O_4$ profiles extracted by the different groups (and for those derived from the US standard atmosphere and the profiles extrapolated from the surface values; see Sect. 4.1) are compared to those for the MPIC $O_4$ profiles (using the standard settings). The corresponding ratios are shown in Fig. A6 and Table A4 in Appendix A4.
ically < 2 %). For the US standard atmosphere, larger deviations (up to 7 %) are derived.

Next the effect of the aerosol extinction profile is investigated. In this study, aerosol extinction profiles are derived from the combined ceilometer and sun photometer measurements (see Table 5). In short, the ceilometer measurements of the attenuated backscatter are scaled by the simultaneously measured AOD from the sun photometer to obtain the aerosol extinction profile. Also, the self-attenuation of the aerosol is taken into account. The different steps are illustrated in Fig. 8 and described in detail in Appendix A5. In the extraction procedure, several assumptions have to be made: first, the ceilometer profiles have to be extrapolated for altitudes below 180 m, for which the ceilometer is not sensitive. Furthermore, they have to be averaged over several hours and are in addition vertically smoothed (above 2 km) to minimise the rather large scatter. Finally, above 5 to 6 km (depending on the ceilometer profiles) the extinction is set to zero because of the further increasing scatter and the usually small extinctions. This assumption reflects a practical limitation of the ceilometer likely responsible for the larger variability in the profile shape aloft by different groups. Another assumption is that the Ångström exponent and the lidar ratio are independent of altitude, which is typically not strictly fulfilled (the lidar ratio describes the ratio between the extinction and backscatter probabilities of the molecules and aerosol particles).

These uncertainties are quantified by sensitivity studies, in particular the effect of the extrapolation below 180 m and the altitude above which the aerosol extinction is set to zero. Other uncertainties, like the effect of the assumption of a constant lidar ratio, are more difficult to quantify without further information (see below). The effect of temporal averaging and smoothing is probably negligible for 8 July, because similar height profiles are found for all three periods of that day, but on 18 June the effect might be more important.

Figure 9 shows a comparison of the aerosol extinction profiles extracted by the different groups for the three periods on both days. Especially on 8 July, systematic differences are found. They are caused by the different altitudes above which the aerosol extinction is set to zero. In combination with the scaling of the profiles with the AOD obtained from the sun photometer, this also influences the extinction values close to the surface. Deviations up to 18 % are found for the first period of 8 July. These deviations also have an effect on the corresponding O₄ (d)AMFs, where higher values are obtained for the profiles (INTA and IUPB 300 m) which were extracted for a larger altitude range (Fig. A7 and Table A5 in Appendix A4). Here it is interesting to note that these differences are not related to the direct effect of the aerosol extinction at high altitude but to the corresponding (via the scaling with the AOD) decrease in the aerosol extinction close to the surface. Larger deviations (up to 4 %) are found for 8 July, while the deviations on 18 June are within 3 %. This effect is further examined in Appendix A6.

In Fig. A8 and Table A6 in Appendix A4, the effect of the different extrapolations of the aerosol extinction profile below 180 m on the O₄ (d)AMFs is quantified. Similar deviations (up to 5 %) are found for both days.

Finally, we investigated the effect of changing aerosol optical properties with altitude (changing lidar ratio). Such effects are particularly important if the wavelength of the ceilometer measurements (1064 nm) differs largely from that of the MAX-DOAS observations (360 nm). Based on the partitioning into fine- and coarse-mode aerosols (derived from the sun photometer observations) and the corresponding phase functions and optical depths, the sensitivity of the ceilometer to fine-mode aerosols was estimated (for details see Appendix A5). While for 18 June the contribution of the fine mode to the ceilometer signal is about 32 % on 8 July it is much larger (about 82 %). Thus, it can be concluded that the aerosol extinction profile derived from the ceilometer is largely representative of the fine-mode aerosols on that day.

To investigate the effect of the remaining uncertainties, the shape of the aerosol extinction profile was further modified (for details see Appendix A5) while taking into account that the coarse aerosols are typically located at low altitudes. The corresponding repartitioning of the aerosol extinction profile led to a decrease in the aerosol extinction close to the surface, which is balanced by an increase at higher altitudes (see Fig. A34). The O₄ dAMFs calculated for the modified profile are larger than those for the standard settings by about 17 % (for details see Appendix A5).

The effect of elevated aerosol layers (see Ortega et al., 2016) was further investigated by systematic sensitivity studies (Appendix A6). On both selected days enhanced aerosol extinction was found at elevated layers (Fig. 9). Compared to those reported by Ortega et al. (2016) the profiles extracted in this study reach up to even higher altitudes. For the investigation of the effect of changes in the aerosol extinction at different altitudes, the aerosol extinction profile on 8 July was subdivided into three layers (0–1.7, 1.7–4.9, 4.9–7 km), and the extinction in the individual layers was increased by +40 %. It was found that even a strong increase in the aerosol extinction at high altitudes by 40 % leads only to an increase in the O₄ dAMFs of 7 %.

Also, the effect of horizontal gradients should be briefly discussed. For the selected periods of both days, the wind direction and wind speed were rather constant. On 18 June the wind direction was between 80 and 150° with respect to north, and the wind speed was about 2 m s⁻¹. On 8 July the wind direction was between 70 and 90° (the wind came from almost the same direction at which the instruments were looking), and the wind speed was about 3 m s⁻¹. During the 4 h of the selected period on 8 July, the air masses moved over a distance of about 40 km. During the 3 h of the selected period on 18 June, the air masses moved over a distance of about 20 km. These distances are larger than the distances to which the MAX-DOAS observations are sensitive (about 5–15 km). Since the AOD and the aerosol extinction profiles

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were also rather constant during both selected periods, we concluded that for the measurements considered here, horizontal gradients can be neglected. It should also be noted that the discrepancies between measurements and simulations were simultaneously observed at all four azimuth directions.

In Fig. A9 and Table A7 in Appendix A4, the effect of different single scattering albedos (between 0.9 and 1) on the O$_4$ (d)AMFs is quantified. The effect on the O$_4$ (d)AMFs is up to 4% on 18 June and up to 2% on 8 July 2013.

The impact of the aerosol phase function is investigated in two ways: first, simulation results are compared for Henyey–Greenstein phase functions with different asymmetry parameters. The corresponding results are shown in Fig. A10 and Table A8 in Appendix A4. The differences in the O$_4$ (d)AMFs for the different aerosol phase functions are rather strong: up to 3% for the O$_4$ AMFs and up to 8% for the O$_4$ dAMFs (larger uncertainties for the dAMFs are found because of the strong influence of the phase function on the 90° observations). Here it should be noted that the actual deviations from the true phase function might be even larger. In order to better estimate these uncertainties, simulations for phase functions derived from the sun photometer measurements based on Mie theory (in the following referred to as Mie phase functions) were also performed. A comparison of these Mie phase functions with the Henyey–Greenstein phase functions is shown in Fig. 10. Large differences, especially in the forward direction, are obvious. The O$_4$ (d)AMFs for the Mie phase functions are compared to the standard simulations (using the HG phase function for an asymmetry parameter of 0.68) in Fig. A11 and Table A9 in Appendix A4.

Again, rather large deviations are found, which are larger on 18 June (up to 9%) than on 8 July (up to 5%).

In Fig. A12 and Table A10 in Appendix A4, the effect of different surface albedos on the O$_4$ (d)AMFs is quantified. For the considered variations (0.03 to 0.1) the changes in the O$_4$ (d)AMFs are within 2%.

4.2.2 Uncertainties of the O$_4$ (d)AMFs caused by imperfections in the radiative transfer models

The radiative transfer models used in this study are well established and showed very good agreement in several inter-comparison studies (e.g. Hendrick et al., 2006; Wagner et al., 2007; Lorente et al., 2017). Nevertheless, they are based on different methods and use different approximations (e.g. with respect to the Earth’s sphericity). Thus, we compared the simulated O$_4$ (d)AMFs for both days in order to estimate the uncertainties associated with these differences. In Fig. A13 and Table A11 (Appendix A4), the comparison results are shown. They agree within a few percent with slightly larger differences for 18 June (up to 6%) than for 8 July (up to 3%).

So far, all radiative transfer simulations were carried out without considering polarisation. Thus, in Fig. A14 and Table A12 in Appendix A4, the results with and without considering polarisation are compared. The corresponding differences are very small (< 1%).
Figure 9. Comparison of the aerosol extinction profiles extracted by the different groups for all three periods on both days.

Figure 10. Comparison of different aerosol phase functions used in the radiative transfer simulations. Panel (b) is a close-up of (a).

4.2.3 Summary of uncertainties of the O$_4$ AMF from radiative transfer simulations

Table 9 presents an overview of the different sources of uncertainties of the simulated O$_4$ (d)AMFs derived from the comparison of the results from different groups and the sensitivity studies. The uncertainties are expressed as relative deviations from the results for the standard settings (see Table 6) derived by MPIC using McArtim.

In general, larger uncertainties are found for the O$_4$ dAMFs compared to the O$_4$ AMFs. This is expected because the uncertainties of the O$_4$ dAMFs contain the uncertainties of two simulations (at 90° elevation and at low elevation). Another general finding is that the uncertainties on 18 June
are larger than on 8 July. This finding is mainly related to the larger uncertainties due to the aerosol phase function, which has an especially strong forward peak on 18 June. Also, the uncertainties from the \( \text{O}_4 \) profile extraction, the choice of the radiative transfer model and the extrapolation of the aerosol extinction below 180 m are larger on 18 June than on 8 July. These higher uncertainties are probably mainly related to the high aerosol extinction close to the surface on 18 June (see Sect. 5.1 and Appendices A2 and A5).

For the total uncertainties two values are given in Table 9: the average deviation is the sum of all systematic deviations of the individual uncertainties (the corresponding mean of the maximum and minimum values). The second quantity (the range of uncertainties) is calculated from half the individual uncertainty ranges by assuming that they are independent.

Finally, it should be noted that for some uncertainties (e.g. the effects of the surface albedo or the single-scattering albedo) the given numbers probably overestimate the true uncertainties, while for others, for example, the uncertainties related to the aerosol extinction profiles or the phase functions they possibly underestimate the true uncertainties (although reasonable assumptions were made). The two latter uncertainties are especially large for 18 June. The differences between the days are discussed in more detail in Sect. 5.

4.3 Uncertainties of the spectral analysis

The uncertainties of the spectral analysis are caused by different effects:

- the specific settings of the spectral analysis like the fit window or the degree of the polynomial, particularly the effect of choosing different \( \text{O}_4 \) cross sections as well as their temperature dependence;
- the properties (and imperfections) of the \text{MAX-DOAS} instruments;
- the effect of different analysis software and implementations;
- the effect of the wavelength dependence of the AMF across the fit window.

These uncertainties are discussed and quantified in the following subsections.

| Effects of RTM | \( \text{O}_4 \) AMF | \( \text{O}_4 \) dAMF |
|---------------|---------------------|---------------------|
| Radiative transfer model | \(-1\%+/2\%\) | \(-1\%+/5\%\) |
| Polarisation | \(0\%/0\%\) | \(0\%/0\%\) |

**Effects of input parameters**

| \( \text{O}_4 \) profile extraction | \(0\%+/2\%\) | \(0\%+/4\%\) |
| Single-scattering albedo | \(-1\%+/3\%\) | \(-1\%+/3\%\) |
| Phase function | \(-3\%+/3\%\) | \(-5\%+/9\%\) |
| Aerosol profile extraction | \(-1\%+/1\%\) | \(-2\%+/4\%\) |
| Extrapolation below 180 m | \(0\%+/2\%\) | \(-1\%+/4\%\) |
| Lidar ratio and wrong wavelength | not quantified | not quantified |
| Surface albedo | \(0\%+/2\%\) | \(0\%+/2\%\) |

**Total uncertainty**

| Average deviation (from results for standard settings) | \(+4.5\%\) | \(+8.5\%) |
| Range of uncertainty | \(\pm 4.4\%\) | \(\pm 4.7\%\) |

\(\text{a}\) This uncertainty does not contain the contribution from variation of aerosol properties with altitude; see text.

\(\text{b}\) Uncertainty was not assessed for 18 June 2013, because the contributions from the coarse and fine mode at both wavelengths are very different (see Table A28). The uncertainty is thus much larger than on 8 July 2013.

\(\text{c}\) This was only the case if lidar profiles at the same wavelength and without gaps in the troposphere were available.
4.3.1 Comparison of O₄ (d)AMFs derived from the synthetic spectra with O₄ (d)AMFs directly obtained from the radiative transfer simulations

Synthetic spectra for both selected days were simulated using the radiative transfer model SCIAMACHY (for details see Sect. 2.4 and Table A3 in Appendix A1). While spectra for the whole day are simulated (for the viewing geometry see Table A2 in Appendix A1) it should be noted that the aerosol properties during the middle periods are also used for the whole day (to minimise the computational efforts). The spectra are analysed using the standard settings and the derived O₄ (d)SCDs are converted to O₄ (d)AMFs using Eq. (1). In addition to the spectra, O₄ (d)AMFs at 360 nm are simulated directly by the RT models using exactly the same settings. These O₄ (d)AMFs are used to test whether the spectral retrieval results are indeed representative of the simulated O₄ (d)AMFs at 360 nm.

Spectra are simulated with and without considering the temperature dependence of the O₄ cross section. Also, one version of synthetic spectra with added random noise is processed.

First, the synthetic spectra are analysed using the standard settings (see Table 7). Examples of the O₄ fits for synthetic (and measured) spectra are shown in Fig. 11. Here it is interesting to note that the ratios of the results for the measured and the simulated spectra are between 0.68 and 0.74, similarly to the ratio for the dAMFs on 8 July shown in Table 8.

In Fig. 12 the ratios of the O₄ (d)AMFs derived from the synthetic spectra vs. those directly obtained from the radiative transfer simulations at 360 nm are shown. In panel (a) the results for synthetic spectra considering the temperature dependence of the O₄ cross section are presented (without noise). Systematically enhanced ratios are found in the morning and evening, while for most of the day the ratios are close to unity. The higher values in the morning and evening are probably partly caused by the increased light paths through higher atmospheric layers (with lower temperatures) when the SZA is high. Interestingly, if the temperature dependence of the O₄ cross section is not taken into account (Fig. 12b), slightly enhanced ratios during the morning and evening are still found, which can no longer be explained by the temperature dependence of the O₄ cross section. Thus, we speculate that part of the enhanced values at high SZA are probably caused by the wavelength dependence of the O₄ AMFs. Nevertheless, for most of the day the ratio is very close to unity, indicating that for SZA < 75° the O₄ (d)AMFs obtained from the spectral analysis are almost identical to the O₄ (dAMFs) directly obtained from the radiative transfer simulations (at 360 nm).

In Fig. 12c results for spectra with added random noise (without consideration of the temperature dependence of the O₄ cross section) are shown. On average similar results to those for the spectra without noise (Fig. 12b) are found but the results now show a large scatter. From these results and the spectral analyses (Fig. 11), we conclude that the noise added to the synthetic spectra overestimates that of the real measurements. For the sensitivity studies discussed in Sect. 4.3.2 only synthetic spectra without noise were used.

In Table A13 in Appendix A4 the average ratios for the middle period on each selected day are shown. They deviate from unity by up to 2% indicating that the wavelength dependence of the O₄ (d)AMF is negligible for the considered cases for SZA < 75°.

4.3.2 Sensitivity studies for different fit parameters

In this section the effect of the choice of several fit parameters on the derived O₄ (d)AMFs is investigated using both measured and synthetic spectra. It should be noted that in the following only synthetic spectra without noise were used, because for the sensitivity studies we are interested in the systematic effects. Only one fit parameter is varied for each individual test, and the results are compared to those for the standard fit parameters (see Table 7).

First the fit window is varied. Besides the standard fit window (352 to 387 nm), which contains two O₄ bands, two fit windows towards shorter wavelengths are also tested: 335–374 nm (including two O₄ bands) and 345–374 nm (including one O₄ band at 360 nm). The ratios of the derived O₄ (d)AMFs vs. those for the standard analysis are shown in Fig. A15 and Table A14 in Appendix A2. On 18 June rather large deviations in the O₄ (d)AMFs are found for both measured (−12 %) and synthetic spectra (−5 %) for the spectral range 335 to 374 nm. On 8 July the corresponding differences are smaller (−6 % and −2 % for measured and synthetic spectra, respectively). For the spectral range 345–374 nm, smaller differences of only up to 1% are found for both days. The reason for the larger deviations on 18 June for the spectral range 335–374 nm is not clear. One possible reason could be the differences between the Ångström parameters (see Fig. 1) and phase functions (see Fig. 10).

In Fig. A16 and Table A15 the results for different degrees of the polynomial used in the spectral analysis are shown. For the measured spectra, systematically higher O₄ (d)AMFs (up to 6%) than for the standard analysis are found when using lower polynomial degrees. For the synthetic spectra the effect is smaller (< 3%).

In Fig. A17 and Table A16 the results for different intensity offsets are shown. Again, for the measured spectra systematically higher O₄ (d)AMFs (up to 16%) than for the standard analysis are found when reducing the order of the intensity offset, while for the synthetic spectra the effect is smaller (< 3%). Higher-order intensity offsets might compensate for wavelength-dependent offsets (e.g. spectral stray light), which can be important for real measurements, while the synthetic spectra do not contain such contributions. In Fig. A18 and Table A17 the results for spectral analyses with only one Ring spectrum are shown. In contrast to the standard analysis, which includes two Ring spectra (one for clear...
Figure 11. Spectral analysis results for a real measurement from the MPIC instrument (left) and a synthetic spectrum with and without noise. Spectra are taken from 8 July 2013 at 11:26 (elevation angle = 1°). The derived O₄ dSCD is shown above the individual plots.

Figure 12. Ratios of the O₄ (d)AMFs derived from synthetic spectra vs. those obtained from radiative transfer simulations at 360 nm for both selected days.

and one for cloudy sky; see Wagner et al., 2009), only the Ring spectrum for clear sky is used. For both selected days, only small deviations are found (within 2%) compared to the standard analysis.

4.3.3 Sensitivity studies using different trace gas absorption cross sections

In this section the impact of different trace gas absorption cross sections on the derived O₄ (d)AMFs is investigated.

In Fig. A19 and Table A18 the results for using two NO₂ cross sections (294 and 220 K) compared to the standard analysis (using only a NO₂ cross section for 294 K) are shown. The results are almost the same as for the standard analysis.

In Fig. A20 and Table A19 the results for using an additional wavelength-dependent NO₂ cross section compared to the standard analysis (using only one NO₂ cross section) are shown. The second NO₂ cross section is calculated by multiplying the original cross section by wavelength (Pukštite et al., 2010). Again, only small deviations are found in the results from the standard analysis (1% for the measured spectra and 2% for the synthetic spectra).

In Fig. A21 and Table A20 results for using and additional wavelength-dependent O₄ cross sections compared to the standard analysis (using only one O₄ cross section) are shown. The second O₄ cross section is calculated like for NO₂ but an orthogonalisation with respect to the original O₄ cross section (at 360 nm) is also performed. The derived O₄ (d)AMFs are almost identical to those from the standard analysis (within 1%).

For the spectral retrieval of HONO in a similar spectral range, a significant impact of water vapour absorption, around 363 nm, was found in Wang et al. (2017a) and Lampel et al. (2017). In Fig. A22 and Table A21 the O₄ results for including a H₂O cross section (Polyansky et al., 2018) com-
pared to the standard analysis (using no H₂O cross section) are shown. The results are almost identical to those from the standard analysis (within 1 %).

In Fig. A23 and Table A22 the results for including a HCHO cross section compared to the standard analysis (using no HCHO cross section) are shown. Especially for 18 June a large systematic effect is found: the O₄ dAMFs are smaller than for the standard analysis for measured and synthetic spectra by 4 % and 6 %, respectively. On 8 July the underestimation is smaller (2 % and 3 % for measured and synthetic spectra).

### 4.3.4 Effect of using different O₄ cross sections

In Fig. A24 and Table A23 the results for different O₄ cross sections are compared to the standard analysis (using the Thalman O₄ cross section). The results for both days are almost identical. For the real measurements, the derived O₄ dAMFs using the Hermans and Greenblatt cross sections are 3 % smaller and 8 % larger than those for the standard analysis, respectively. However, if the Greenblatt O₄ cross section is allowed to shift during the spectral analysis, the overestimation can be largely reduced to only +3 %. This confirms findings from earlier studies (e.g. Pinardi et al., 2013) that the wavelength calibration of the original data sets is not very accurate.

For the synthetic spectra slightly different results to those for the real measurements are found for the Hermans O₄ cross section. The reason for these differences is not clear. However, here it should be noted that the temperature-dependent O₄ absorption in the synthetic spectra does probably not exactly represent the true atmospheric O₄ absorption.

### 4.3.5 Effect of the temperature dependence of the O₄ cross section

The new set of O₄ cross sections provided by Thalman and Volkamer (2013) allows the temperature dependence of the atmospheric O₄ absorptions to be investigated in detail. They provide O₄ cross sections measured at five temperatures (203, 233, 253, 273, 293 K) covering the range of temperatures relevant for atmospheric applications. Using these cross sections, the effect of the temperature dependence of the O₄ absorptions is investigated in two ways:

1. In a first test, synthetic spectra are simulated for different surface temperatures assuming a fixed lapse rate. These spectra are then analysed using the O₄ cross section for 293 K (which is usually used for the spectral analysis of O₄). From this study the magnitude of the effect of the temperature dependence of the O₄ cross section on MAX-DOAS measurements can be quantified.

2. In a second test, measured and synthetic spectra for both selected days are analysed with O₄ cross sections for different temperatures. From this study it can be seen to which degree the temperature dependence of the O₄ cross section can be already corrected during the spectral analysis (if two O₄ cross sections are used simultaneously).

For the first study, MAX-DOAS spectra are simulated in a simplified way:

- Atmospheric temperature profiles are constructed for surface temperatures between 220 and 310 K in steps of 10 K assuming a fixed lapse rate of −0.656 K/100 m.

- For each altitude layer (vertical extension: 20 m below 500 m, 100 m between 500 m and 2 km, 200 m between 2 and 12 km, 1 km above) the O₄ concentrations (calculated from the US standard atmosphere) are multiplied by the corresponding differential box AMFs calculated for typical atmospheric conditions and viewing geometries (see Fig. A25 in Appendix A4).

- The derived high-resolution spectra are convolved with the instrument slit function (FWHM of 0.6 nm).

- The logarithm of the ratio of the spectra for the low elevation and zenith is calculated and analysed using the O₄ cross section for 293 K.

- The derived O₄ DAMFs are divided by the corresponding dAMFs directly obtained from the radiative transfer simulations.

These calculated ratios as a function of the surface temperature are shown in Fig. 13. A strong and systematic dependence on the surface temperature is found (a 15 % change for a change in the surface temperature between 240 and 310 K). However, except for measurements at polar regions, the deviations are usually small. Since for both selected days the temperatures were rather high (indicated by the two coloured horizontal bars in the figure), the effect of the temperature dependence of the O₄ absorption for the middle period of each day is very small (−1 % to −2 % for 18 June and 0 % to +1 % on 8 July). It should be noted that the results shown in Fig. 13 are obtained for generalised settings of the radiative transfer simulations. Thus, it is recommended that future studies should investigate the effect of the temperature dependence in more detail and using the exact viewing geometry for individual observations. However, since the temperatures on both selected days were rather high, for this study the simplifications of the radiative transfer simulations have no strong influence on the derived results.
In the second test the measured and synthetic spectra are analysed using O₄ cross sections for different temperatures. The corresponding results are shown in Fig. A26 and Table A24.

If only the O₄ cross section at low temperature (203 K) is used, the derived O₄ AMFs and dAMFs are about 16% and 30% smaller than for the standard analysis (using the O₄ cross section for 293 K). These results are consistently obtained for the measured and synthetic spectra. If, however, two O₄ cross sections (for 203 and 293 K) are simultaneously included in the analysis, different results are obtained for the measured and synthetic spectra: for the measured spectra the derived O₄ (d)AMFs agree within 4% with those from the standard analysis. In contrast, for the synthetic spectra, the derived O₄ (d)AMFs are systematically smaller (by about 6% to 18%). This finding was not expected, because exactly the same cross sections were used for both the simulation and the analysis of the synthetic spectra. Detailed investigations (see Appendix A4) led to the conclusion that there is a slight inconsistency in the temperature dependence of the O₄ cross sections from Thalman and Volkamer (2013): the ratio of the peak values of the cross section at 360 and 380 nm changes in a non-continuous way between 253 and 233 K (see Fig. A27 in Appendix A4); see also Fig. S2 (values for 380 nm) in the supplementary material of Thalman and Volkamer (2013). The reason for this inconsistency is currently not known. If these two O₄ bands are included in the spectral analysis (as for the standard settings), the convergence of the spectral analysis strongly depends on the ability to fit both O₄ bands well. Thus, the fit results for both O₄ cross sections are mainly determined by the relative strengths of both O₄ bands (see Fig. A27 in Appendix A4). If instead a smaller wavelength range is used containing only one absorption band (345–374 nm), the derived O₄ (d)AMFs are in rather good agreement with the results of the analysis (using only the O₄ cross section for 293 K); see Table A25 in Appendix A4. In that case, the convergence of the fit mainly depends on the temperature dependence of the line width. It should be noted that the non-continuous temperature dependence of the O₄ absorption cross section only affects the analysis of the synthetic spectra, because for the simulation of the spectra all O₄ cross sections for temperatures between 233 and 293 K were used. For the measured spectra, no problems are found, because in the spectral analysis only the O₄ cross sections for 233 and 293 K were used.

In Fig. A28 in Appendix A4 the ratios of both fit coefficients (for 203 and 293 K) are shown, as well as the derived effective temperatures for the analyses of measured and synthetic spectra. For the measured spectra the ratios are close to zero and the derived temperatures are close to 300 K most of the time (except in early morning and evening), because the effective atmospheric temperature for both days is close to the temperature of the high temperature O₄ cross section (293 K) (see Fig. 13). Similar results (at least around noon) are also obtained for the synthetic spectra if the narrow spectral range (345–374 nm) is used. For the standard fit range (including two O₄ bands), however, the ratios are much higher, again indicating the effect of the inconsistency of the temperature dependence of the O₄ cross sections (see Fig. A27 in Appendix A4).

4.3.6 Results from different instruments and analyses by different groups

In this section the effects of using measurements from different instruments and having these spectra analysed by different groups are investigated. For that purpose three different procedures are followed: first, MPIC spectra are analysed by other groups; second, the spectra from other instruments are analysed by MPIC; third, the spectra from non-MPIC instruments are analysed by the respective group.

In Fig. 14a and Table A25 (in Appendix A4) the comparison results of the analysis of MPIC spectra by other groups vs. the analysis of MPIC spectra by MPIC are shown. Especially for 18 June, rather large differences (between −6%/+5%) to the MPIC standard analysis are found. Interestingly the largest differences are found in the morning when the aerosol extinction close to the surface was strongest. On 8 July smaller differences (between −6% and −1%) are found.

In Fig. 14b and Table A25 (in Appendix A4) the comparison results of the analysis of spectra from other instruments by MPIC vs. the analysis of MPIC spectra by MPIC are shown. For this comparison all analyses are performed in the spectral range 335–374 nm, because the standard spectral range (352–387 nm) is not covered by all instruments. Again, the largest differences are found for 18 June (up to ±11%). For 8 July the differences reach up to ±6%, but for this day only a few measurements in the morning are available.

In Fig. 14c and Table A25 (in Appendix A4) the comparison results of the analysis of spectra from other instru-
Figure 14. (a) Ratios of the $O_3$ (d)AMFs derived from MPIC spectra when analysed by other groups vs. those analysed by MPIC for both selected days. (b) Ratios of the $O_3$ (d)AMFs derived from spectra measured by other groups but analysed by MPIC vs. those for the MPIC instrument analysed by MPIC (using the spectral range 335–374 nm for all instruments). (c) Ratios of the $O_3$ (d)AMFs derived from spectra measured and analysed by other groups (using different wavelength ranges and settings) vs. those for the MPIC instrument analysed by MPIC.

ments by the respective group vs. the MPIC analysis by MPIC (standard analysis) is shown. From this exercise the combined effects of different instrumental properties and retrievals can be estimated. Interestingly, the observed differences are only slightly larger than those for the analysis of the spectra from the different instruments by MPIC (Fig. 14b). This indicates that the largest uncertainties are related to the differences in the different instruments and not to the settings and implementations of the different retrievals. For the middle period of 18 June the uncertainties are within 12%. This range is also assumed for 8 July. Here it is interesting to note that the derived uncertainties of the spectral analysis are probably not representative of most recent measurement campaigns. For example, during the CINDI-2 campaign (http://www.tropomi.eu/data-products/cindi-2, last access: 29 April 2019) the deviations in the $O_3$ spectral analysis results were much smaller than for the selected days during the MAD-CAT campaign (Kreher et al., 2019). A summary
Figure 15. Comparison of measured and simulated O₃ (d)AMFs for both selected days. Measurements are from four different instruments but are analysed by MPIC using the standard settings (see Table 7). Simulations are performed by three different groups using Mie phase functions and otherwise the standard settings (see Table 6).
of the comparison of the measurements from different instruments and radiative transfer simulations using different models is given in Fig. 15.

4.3.7 Summary of uncertainties of the $O_4$ AMF from the spectral analysis

Table 10 presents an overview of the different sources of uncertainty of the measured $O_4$ (d)AMFs obtained in the previous subsections. The uncertainties are expressed as relative deviations from the results for the standard settings (see Table 7) derived by MPIC from spectra of the MPIC instrument.

Like for the simulation results, in general, larger uncertainties are found for the $O_4$ dAMFs compared to the $O_3$ AMFs. This is expected because the uncertainties of the $O_4$ dAMFs contain the uncertainties of two analyses (at 90° elevation and at low elevation). Also, the uncertainties on 18 June are again larger than on 8 July. This finding was not expected but is possibly related to the higher gas abundances (see Fig. 1 and Table A3 in Appendix A1) and the higher aerosol extinction close to the surface on 18 June.

Another interesting finding is that the uncertainties of the spectral analysis of $O_4$ are dominated by the effect of instrumental properties up to ±12% in the morning of 18 June. Further important uncertainties are associated with the choice of the wavelength range, the degree of the polynomial and the intensity offset. In contrast, the exact choices of the trace gas cross sections (including their wavelength- and temperature dependencies) play only a minor role (up to a few percent). Excellent agreement (within ±1%) is found in particular for the $O_3$ analysis of the synthetic spectra using the standard settings and the directly simulated $O_4$ (d)AMFs at 360 nm. This indicates that the $O_4$ (d)AMFs retrieved in the wavelength range 352–387 nm are indeed representative of radiative transfer simulations at 360 nm.

As for the uncertainties of the simulated $O_4$ (d)AMFs, the uncertainties of the spectral analysis are also split into a systematic and a random term: the systematic deviations in the $O_4$ dAMFs from those of the standard settings are about +1% and −1.5% for 18 June and 8 July, respectively. The range of uncertainty is calculated from the uncertainty ranges of the different contributions by assuming that they are all independent. The random uncertainty ranges for 18 June and 8 July are calculated as ±12.5% and ±10.8%, respectively.

4.4 Recommendations derived from the sensitivity studies

In this section a short summary of the most important findings from the sensitivity studies is given.

- Temperature and pressure profiles.
  Temperature and pressure profiles from sondes or model data should be used if available. Alternatively, temperature and pressure profiles extrapolated from surface measurements could be used. Typical uncertainties of

the $O_4$ VCD derived from such profiles are still <2%. For high temperatures (<20°C) the atmospheric humidity should be considered. If no measurements are available, prescribed profiles can be used, e.g. from the US standard atmosphere or climatologies of temperature and pressure profiles. However, depending on location and season the uncertainties of the resulting $O_4$ VCD can be rather large (see also Ortega et al., 2016).

- Integration of the $O_4$ VCD
  The integration should be performed on a vertical grid with at least 100 m resolution up to an altitude of 30 km. The surface altitude should be taken into account with an accuracy of at least 20 m.

- Measurements and spectral analysis.
  Instruments should have a small field of view (≤1°), an accurate elevation calibration (better than 0.5°) and a small and preferably well-characterised stray light level. For the data analysis the standard settings provided in Table 7 should be used. From the analysis of synthetic spectra it was found that the results for these settings are consistent with simulated $O_4$ (d)AMFs within 1%.

- Information on aerosols.
  Aerosol profiles should be obtained from lidar or ceilometers using similar wavelengths to the MAX-DOAS measurements if available (see e.g. Ortega et al., 2016). Preferred lidar types are High Spectral Resolution Lidar (HSRL) or Raman lidar, which directly provide profiles of aerosol extinction and thus need no assumptions on the lidar ratio. They should also have high signal-to-noise ratios and a shallow blind region at the surface in order to cover a large altitude range. Information on aerosol optical properties and size distributions from sun photometers or in situ measurements should be used.

- RTM simulations.
  Radiative transfer models should use Mie phase functions and aerosol single-scattering albedo, e.g. derived from sun photometer observations. The consideration of polarisation and rotational Raman scattering is not necessary.

In summary, if the optimised settings described above are used, the uncertainties of the radiative transfer simulations and spectral analysis can be largely reduced: the uncertainties of the $O_4$ dAMFs related to radiative transfer simulations can be reduced from about ±8% as in this study to about ±4%; those related to the spectral analysis can be reduced from about ±10% to about ±6%.
Table 10. Summary of uncertainties of the measured O$_4$ (d)AMFs for the middle period of each selected day. The two numbers left and right of the slash indicate the minimum and maximum deviations. The columns labelled “optimum” indicate the uncertainties which could be reached if optimum instrumental performance was ensured and optimum cross section was available.

|                      | O$_4$ AMF | O$_4$ dAMF |
|----------------------|-----------|------------|
|                      | 18 June   | 8 July     | Optimum | 18 June   | 8 July     | Optimum |
| Consistency spectral analysis vs. RTM |           |            |         |           |            |         |
| Analysis of synthetic spectra | $-1\%$/$+1\%$ | $-1\%$/$0\%$ | $\pm1\%$ | $0\%$/$0\%$ | $0\%$/$+1\%$ | $\pm1\%$ |
| Fit settings          |           |            |         |           |            |         |
| Spectral range        | $-7\%$/$-3\%$ | $-3\%$/$0\%$ | $\pm1\%$ | $-12\%$/$-1\%$ | $-6\%$/$-1\%$ | $\pm1\%$ |
| Degree of polynomial  | $+0\%$/$+4\%$ | $0\%$/$+3\%$ | $\pm1\%$ | $0\%$/$+6\%$ | $0\%$/$+6\%$ | $\pm1\%$ |
| Intensity offset$^a$  | $+1\%$/$+5\%$ | $+1\%$/$+3\%$ | $\pm1\%$ | $+3\%$/$+11\%$ | $+2\%$/$+4\%$ | $\pm1.5\%$ |
| Ring                  | $+1\%$/$+2\%$ | $-1\%$/$+1\%$ | $\pm1\%$ | $+1\%$/$+1\%$ | $-1\%$/$+1\%$ | $\pm1.5\%$ |
| Temperature dependence of NO$_2$ absorption | $0\%$/$0\%$ | $0\%$/$0\%$ | $0\%$ | $0\%$/$0\%$ | $0\%$/$0\%$ | $0\%$/$0\%$ |
| Wavelength dependence of NO$_2$ absorption | $-1\%$/$0\%$ | $0\%$/$0\%$ | $0\%$ | $-2\%$/$-1\%$ | $-1\%$/$0\%$ | $0\%$ |
| Wavelength dependence of O$_4$ absorption | $-1\%$/$0\%$ | $-1\%$/$-1\%$ | $0\%$ | $0\%$/$+1\%$ | $-1\%$/$-1\%$ | $0\%$ |
| Including H$_2$O cross section | $0\%$/$0\%$ | $0\%$/$0\%$ | $0\%$ | $+1\%$/$+1\%$ | $+1\%$/$+1\%$ | $0\%$ |
| Including HCHO cross section | $-3\%$/$0\%$ | $-1\%$/$0\%$ | $0\%$ | $-6\%$/$-4\%$ | $-3\%$/$-2\%$ | $0\%$ |
| Different O$_4$ cross sections$^b$ | $-2\%$/$+1\%$ | $-2\%$/$+1\%$ | $\pm2\%$ | $-3\%$/$+3\%$ | $-3\%$/$+3\%$ | $\pm2\%$ |
| Temperature dependence of the O$_4$ absorption |           |            |         |           |            |         |
| Analysis using two O$_4$ cross sections for different temperatures$^c$ | $0\%$/$0\%$ | $+2\%$/$+2\%$ | $\pm1\%$ | $+4\%$/$+4\%$ | $+1\%$/$+1\%$ | $\pm1.5\%$ |
| Analysis of synthetic spectra for different surface temperatures | $-1\%$/$0\%$ | $-1\%$/$+2\%$ | $\pm4\%$/$+4\%$ | $+1\%$/$+1\%$ | $\pm1\%$ |
| Analysis from different instruments and groups |           |            |         |           |            |         |
| Different groups and analyses$^d$ | $-6\%$/$+5\%$ | $-6\%$/$+5\%$ | $\pm3\%$ | $-12\%$/$+7\%$ | $-12\%$/$+7\%$ | $\pm4.5\%$ |
| Total uncertainty     |           |            |         |           |            |         |
| Average deviation (from results for standard settings) | $-4.5\%$ | $-0.5\%$ | $\pm1\%$ | $-1\%$ | $-1.5\%$ | $\pm1\%$ |
| Range of uncertainty  | $\pm7.0\%$ | $\pm6.5\%$ | $\pm4.2\%$ | $\pm12.5\%$ | $\pm10.8\%$ | $\pm5.7\%$ |

$^a$ Here the case “no offset” is not considered.
$^b$ Here the case of the non-shifted Greenblatt O$_4$ cross section is not considered.
$^c$ Here only the results for the measured spectra in the spectral range 352–387 nm are considered (temperatures on 18 June: 27–31 °C; 8 July: 20–30 °C).
$^d$ The results for 18 June are also taken for 8 July due to the lack of measurements on 8 July.
$^e$ See Kreher et al. (2019).

Preferred scenarios for future studies

In addition to the recommendations given above, future campaigns should aim to cover different meteorological conditions (e.g. low temperatures), viewing geometries (e.g. low SZA), surface albedos (e.g. snow and ice) and wavelengths (e.g. 477, 577 and 630 nm). Also, different aerosol scenarios including those with low AOD should be covered. MAX-DOAS measurements should be performed by at least 2 instruments but preferably more. In order to minimise the effects of instrumental properties, the instruments should be well calibrated and should have low stray light levels. Measurements obtained during the CINDI-2 campaign are probably well suited for a similar study.

5 Comparison of measurements and simulations

The comparison results for both days are different: on 18 June (except in the evening) measurements and simulations agree within uncertainties (the ratio of simulated and measured O$_4$ dAMFs for the middle period of that day is 1.01 ± 0.16). In contrast, on 8 July, measurements and simulations significantly disagree: taking into account the uncertainties of the VCD calculation (3 %), the radiative transfer
simulations (+16 ± 6.4%) and the spectral analysis (−1.5 ± 10.8%) for the middle period of that day results in a ratio of simulated and measured O4 dAMFs of 0.82 ± 0.10, which differs significantly from unity.

5.1 Important differences between the days

On both selected days similar aerosol AODs were measured. Also, the diurnal variation of the SZA was similar because of the proximity to the summer solstice. However, many differences are also found for the 2 selected days, which are discussed below.

1. Temperature, pressure and wind.

On 18 June surface pressure was lower by about 13 hPa and surface temperature was higher by about 7 K than on 8 July, respectively. These differences were explicitly taken into account in the calculation of the O4 profiles or VCDs, the radiative transfer simulations and the interpretation of the spectral analyses. Thus, they are very unlikely to explain the different comparison results on the 2 selected days.

On both days, wind was mainly blowing from east–north-east, but on 18 June it was blowing from the west before about 08:00 and after 20:00 UTC. Wind speeds were lower on 18 June (between 1 and 2 m s\(^{-1}\)) than on 8 July (between 1 and 3 m s\(^{-1}\)).

2. Aerosol properties.

The in situ aerosol measurements show very different abundances and properties of aerosols close to the ground for the selected days. On 18 June much higher concentrations of larger aerosol particles are found, which cannot be measured by the ceilometer due to the blindness for the lowest 180 m. Thus, it can be concluded that the enhanced aerosol concentration on 18 June is confined to a shallow layer at the surface. In general the aerosol concentrations close to the surface are more variable on 18 June than on 8 July. The high aerosol concentrations close to the surface probably also affect the lidar ratio, which is thus probably more variable on 18 June. Similarly, the phase function derived from the sun photometer (for the integrated aerosol profile) is also probably less representative of the low-elevation angles on 18 June because different aerosol size distributions probably existed at different altitudes. Finally, the Ångström parameter derived from AERONET observations is different for both days, especially for large wavelengths, which is in qualitative agreement with the higher in situ aerosol concentrations of large particles on 18 June. Also, a larger forward peak of the derived aerosol phase function is found for 18 June. Both effects probably cause larger uncertainties on 18 June.

3. Spectral analysis.

Larger uncertainties of the spectral analysis are found for 18 June compared to 8 July. This finding was surprising but was also partly reproduced by the analysis of the synthetic spectra. One possible explanation is the smaller wavelength dependence of aerosol scattering at low altitudes on 18 June, which mainly affects measurements at low-elevation angles. When analysed vs. a zenith reference, for which the broadband wavelength dependency is much stronger (because of the larger contribution from Rayleigh scattering), larger deviations can be expected (e.g. because of differences in instrumental stray light, or the different detector saturation levels). On 18 June higher (about doubled) NO\(_2\) and HCHO concentrations are also present compared to 8 July, possibly leading to increased spectral interferences with the O4 absorption, but this effect is expected to be small.

5.2 Which conditions would be needed to bring measurements and simulations on 8 July into agreement

This section tentatively describes possible (although generally unrealistic) changes in the atmospheric scenario, the instrument properties or the input parameters, which could bring measurements and simulations on 8 July into agreement. If, for example, the whole aerosol extinction profile was scaled by 0.65, the corresponding O4 dAMFs would almost perfectly match the measured ones.

A similarly good agreement could also be achieved if about 27% of the total AOD was shifted from low layers (below 1.68 km) to high layers (above 4.9 km; see Appendix A6). However, in this scenario, about 73% of the total aerosol extinction would be above 1.68 km. Such a scenario would not be in agreement with the AERONET inversion products and would also lead to an underestimation of the diurnal variation of the O4 AMFs measured in zenith direction.

Also, horizontal gradients of the aerosol extinction could in principle explain the discrepancy. While we are not able to quantify them, they surely would have to be of the order of several tens of percent per 10 km. Such persistent horizontal gradients are not supported by the almost constant AOD during the day (and also by the consistent aerosol in situ observations at the different sites). Also, the mismatch between measurements and simulations that is found for all azimuth angles indicates that horizontal gradients can not explain the observed discrepancies.

Another possibility would be aerosol phase functions with very high asymmetry parameters (> 0.75). Also, systematic errors of the O4 cross section could explain the observed discrepancies. Finally, an overcorrection of spectrograph stray light (or any other intensity offset) could explain the dis-
crepancies. However, a rather high overcorrection (by about 20\%) would be needed, which is probably unrealistic.

6 Conclusions

We compared MAX-DOAS observations of the atmospheric O$_4$ absorption with corresponding radiative transfer simulations for 2 mainly cloud-free days during the MAD-CAT campaign. A large part of this study is dedicated to the extraction of input information for the radiative transfer simulations and the quantification of the associated uncertainties of the radiative transfer simulations and spectral retrievals. An important result from the sensitivity studies is that the O$_4$ results derived from the analysis of synthetic spectra using the standard settings are consistent within uncertainties of the VCD calculation (3\%), the radiative transfer simulations (+16\%\% and the spectral analysis (−1.5\%\% for the middle period of that day results in a ratio of simulated and measured O$_4$ dAMFs of 0.82\%\%\% which differs significantly from unity. So far no plausible explanation for the observed discrepancies on 8 July was found.

However, as long as the reason for this deviation is not understood, it is unclear how representative these findings are for other measurements (e.g. from other platforms, at other locations or seasons, for other aerosol loads and other wavelengths). Thus, further studies spanning a larger variety of measurement conditions and including other wavelengths are recommended. The MAX-DOAS measurements collected during the recent CINDI-2 campaign are probably well suited for that purpose.

Data availability. The data used in this study are available at: http://joseba.mpch-mainz.mpg.de/Comparison.htm (last access: 29 April 2019).
Appendix A

A1 Settings used for the simulation of synthetic spectra

Table A1. Vertical resolution used in radiative transfer simulations for different altitude ranges.

| Lower boundary (km) | Upper boundary (km) | Vertical resolution (km) |
|---------------------|---------------------|-------------------------|
| 0                   | 0.5                 | 0.02                    |
| 0.5                 | 2                   | 0.1                     |
| 2                   | 12                  | 0.2                     |
| 12                  | 25                  | 1                       |
| 25                  | 45                  | 2                       |
| 45                  | 100                 | 5                       |
| 100                 | 1000                | 900                     |

Table A2. Dependence of SZA and RAZI on time (UTC) for the standard viewing direction (51° with respect to north).

| Time (UTC) | SZA  | RAZI |
|------------|------|------|
| 03:19      | 90   | −0.1 |
| 04:00      | 85   | 7.7  |
| 04:36      | 80   | 14.2 |
| 05:42      | 70   | 26   |
| 06:44      | 60   | 37.5 |
| 07:48      | 50   | 50.1 |
| 08:54      | 40   | 66.2 |
| 10:16      | 30   | 94.6 |
| 11:26      | 26   | 129  |
| 12:40      | 30   | 163.3|
| 14:02      | 40   | 191.8|
| 15:09      | 50   | 207.9|
| 16:11      | 60   | 220.5|
| 17:14      | 70   | 232  |
| 18:20      | 80   | 243.8|
| 18:56      | 85   | 250.3|
| 19:38      | 90   | 258  |
Table A3. Trace gas profiles and cross sections used for the simulation of the synthetic spectra.

| Trace gas | Vertical profile | Cross section (reference and T) |
|-----------|------------------|---------------------------------|
| O$_4$     | Derived from temperature and pressure profiles: | Thalman and Volkamer (2013) |
|           | 18 Jun: average profiles 11:00–14:00 | (203, 233, 273, 293 K)$^a$ |
|           | 8 Jul: average profiles 07:00–11:00 | (298 K) |
| HCHO      | 18 Jun: 0–1000 m, constant concentration of $2 \times 10^{11}$ molecules cm$^{-3}$ (about 8 ppb) | Meller and Moortgat (2000) |
|           | 8 Jul: 0–1000 m, constant concentration of $1 \times 10^{11}$ molecules cm$^{-3}$ (about 4 ppb) | (298 K) |
| NO$_2$    | Troposphere: | Vandaele et al. (1997) |
|           | 18 Jun: 0–500 m, constant concentration of $4 \times 10^{11}$ molecules cm$^{-3}$ (about 16 ppb) | (220, 294 K) |
|           | 8 Jul: 0–500 m, constant concentration of $2 \times 10^{11}$ molecules cm$^{-3}$ (about 8 ppb) | (220, 294 K) |
|           | Stratosphere: Gaussian profile with maximum at 25 km and FWHM of 16 km, VCD = $5 \times 10^{15}$ molecules cm$^{-2}$ | |
| O$_3$     | Troposphere (0–8 km): | Serdyuchenko et al. (2014) |
|           | constant concentration $6 \times 10^{11}$ molecules cm$^{-3}$ (about 24 ppb) | (193–293 K in steps of 10 K)$^b$ |
|           | Stratosphere: Gaussian profile with maximum at 22 km and FWHM of 15 km, VCD = 314 DU | |

$^a$ The temperature dependence is either considered or a constant temperature of 293 K is assumed (see text for details).

$^b$ The temperature dependence was parameterised according to Paur and Bass (1984).

**Figure A1.** Tropospheric VCDs of NO$_2$ (blue) and HCHO (red) derived from measurements at 30° elevation using the geometric approximation.
A2  Comparison of measured and simulated O$_4$ (d)AMFs for all azimuth and elevation angles of the MPIC MAX-DOAS measurements

The settings for the simulation of the synthetic spectra are given in Table 6 and Tables A1, A2 and A3 in Appendix A1. Measurements are analysed using the standard settings (see Table 7).

Figure A2. Azimuth viewing directions of the four telescopes (T1 to T4) of the MPIC MAX-DOAS instrument. The azimuth angles are defined with respect to north (© Google maps).
For T1 and T4 azimuth direction, no measurements at 1° elevation were possible due to obstacles.

Figure A3.
Figure A3.
Figure A3.
Figure A3. (a) Comparison results for 1° elevation angles on 8 July 2013. The upper lines indicate the O₄ AMFs; the lower lines indicate the O₄ dAMFs (see also Figs. 2 and 3). (b) Comparison results for 3° elevation angles on 8 July 2013. (c) Comparison results for 6° elevation angles on 8 July 2013. (d) Comparison results for 10° elevation angles on 8 July 2013. (e) Comparison results for 15° elevation angles on 8 July 2013. (f) Comparison results for 30° elevation angles on 8 July 2013. (g) Comparison results (only O₄ AMFs) for 90° elevation angles on 8 July 2013.
T1 North-west

For T1 and T4 azimuth direction, no measurements at 1° elevation were possible due to obstacles.

In the following figures, the green lines indicate the results for the modified aerosol profile.

T4 South-west

For T1 and T4 azimuth direction, no measurements at 1° elevation were possible due to obstacles.
Figure A4.
Figure A4. (a) Comparison results for 1° elevation angles on 18 June 2013 including the RTM results for the modified aerosol extinction profile (green line). (b) Comparison results for 3° elevation angles on 18 June 2013. (c) Comparison results for 6° elevation angles on 18 June 2013. (d) Comparison results for 10° elevation angles on 18 June 2013. (e) Comparison results for 15° elevation angles on 18 June 2013. (f) Comparison results for 30° elevation angles on 18 June 2013. (g) Comparison results (only O4 AMFs) for 90° elevation angles on 18 June 2013.
A3 Comparison of the different procedures to extract height profiles of temperature, pressure and O₄ concentration

A3.1 Extraction of temperature and pressure profiles

For the 2 selected days during the MAD-CAT campaign two data sets of temperature and pressure are available: surface measurements close to the measurement site and vertical profiles from ECMWF ERA-Interim reanalysis data (see Table 5). Both data sets are used to derive the O₄ concentration profiles for the three selected periods on both days. The general procedure is that first the temperature profiles are determined. In a second step, the pressure profiles are derived from the temperature profiles and the measured surface pressure. For the temperature profile extraction, three height layers are treated differently:

- **Below 1 km.**
  Between the surface (≈ 150 m above sea level) and 1 km, the temperature is linearly interpolated between the average of the in situ measurements of the respective period and the ECMWF data at 1 km (see next paragraph). This procedure is used to account for the diurnal variation of the temperature close to the surface. Here it is important to note that for this near-surface layer the highest accuracy is required, because (a) the maximum O₄ concentration is located near the surface, and (b) the MAX-DOAS measurements are most sensitive close to the surface.

- **From 1 to 20 km.**
  In this altitude range, the diurnal variation of the temperature becomes very small. Thus, the average of the four ECMWF profiles of each day is used (for simplicity, a sixth-order polynomial is fitted to the ECMWF data).

- **Above 20 km.**
  In this altitude range the accuracy of the temperature profile is not critical and thus the ECMWF temperature profile for 00:00 UTC of the respective day is used for simplicity.

The temperature profiles for 8 July 2013 extracted in this way are shown in Fig. 4 (left). Close to the surface the temperature variation during the day is about 10 K.

In the next step, the pressure profiles are determined from the surface pressure (obtained from the in situ measurements) and the extracted temperature profiles according to the ideal gas law. In principle the effect of atmospheric humidity could also be taken into account, but the effect is very small for near-surface layers and is thus ignored here. The derived pressure profiles for 8 July 2013 are shown in Fig. 4 (right). Excellent agreement with the corresponding ECMWF pressure profiles is found.

Here it should be noted that in principle the ECMWF pressure profiles could also be used. However, we chose to determine the pressure profiles from the surface pressure and the extracted temperature profiles, because this procedure can also be applied if no ECMWF data (or other information on temperature and pressure profiles) are available.

If no profile data (e.g. from ECMWF) are available, temperature and pressure profiles can also be extrapolated from surface measurements, e.g. by assuming a constant lapse rate of −0.65 K/100 m for the altitude range between the surface and 12 km, and a constant temperature above 12 km (as stated above, uncertainties at this altitude range have only a negligible effect on the O₄ VCD). If no measurements or model data are available at all, a fixed temperature and pressure profile can be used, e.g. the US standard atmosphere (United States Committee on Extension to the Standard Atmosphere, 1976).

A3.2 Determination of the uncertainties of the O₄ profiles and O₄ VCDs caused by uncertainties of the input parameters

The uncertainties of the O₄ profiles and O₄ VCDs are derived by varying the input parameters according to their uncertainties. The following results are obtained:

- The variation of the temperature (whole profile) by about 2 K leads to variations of the O₄ concentration (or O₄ VCD) by about 0.8 %.

- The variation of the surface pressure by about 3 hPa leads to variations of the O₄ concentration (or O₄ VCD) by about 0.7 %.

- The effect of uncertainties of the relative humidity depends strongly on temperature: for surface temperatures of 0, 10, 20, 30 and 35 ºC a variation of the relative humidity of 30 % leads to variations of the O₄ concentration (or O₄ VCDs) of about 0.15 %, 0.3 %, 0.6 %, 1.2 % and 1.6 %, respectively. If the effect of atmospheric humidity is completely ignored (dry air is assumed), the resulting O₄ concentrations (or O₄ VCDs) are systematically overestimated by about 0.3 %, 0.7 %, 1.3 %, 2.5 % and 4 % for surface temperatures of 0, 10, 20, 30 and 35 ºC, respectively (assuming a relative humidity of 70 %). In this study we used the relative humidity measured by the in situ sensors. We took these values not only for the surface layers but also for the whole troposphere. Here it should be noted that the related uncertainties of the absolute humidity decrease quickly with altitude because the absolute humidity itself decreases quickly with altitude. Since both selected days were warm or even hot summer days, we estimate the uncertainties of the O₄ concentration and O₄ VCDs due to uncertainties of the relative humidity to 1 % and 0.4 % on 18 June and 8 July, respectively.
Assuming that the uncertainties of the three input parameters are independent, the total uncertainty related to these parameters is estimated to be about 1.5%. 

Figure A5.
Figure A5. (a) Left: Comparison of temperature profiles extracted by the different groups (also shown are the profiles from the US standard atmosphere and the profiles extrapolated from the surface measurements). Right: Differences in these profiles compared to the MPIC standard extraction. (b) Left: Comparison of pressure profiles extracted by the different groups (also shown are the profiles from the US standard atmosphere and the profiles extrapolated from the surface measurements). Right: Differences in these profiles compared to the MPIC standard extraction. (c) Left: Comparison of $O_4$ concentration profiles extracted by the different groups (also shown are the profiles from the US standard atmosphere and the profiles extrapolated from the surface measurements). Right: Differences in these profiles compared to the MPIC standard extraction.
A4 Results of the sensitivity studies of simulated and measured O₄ (d)AMFs

Figure A6. Ratios of the O₄ AMFs (a, b) and O₄ dAMFs (c, d) derived for different O₄ profiles vs. the standard O₄ profile (MPIC) for both selected days. Besides the results for O₄ profiles extracted by the different groups, the results for O₄ profiles derived from the US standard atmosphere and for the extrapolation of the surface values are included.

Table A4. Average ratios of O₄ (d)AMFs simulated for different O₄ profiles vs. the results for the standard settings (using the MPIC O₄ profiles) for the middle periods on each selected day.

| O₄ profile     | AMF ratios  | dAMF ratios |
|----------------|-------------|-------------|
|                | 18 June 2013 | 8 July 2013 | 18 June 2013 | 8 July 2013 |
|                | 11:00–14:00 | 07:00–11:00 | 11:00–14:00 | 07:00–11:00 |
| MPIC-2         | 1.00        | 1.00        | 1.00         | 1.00         |
| INTA           | 1.01        | 1.01        | 1.02         | 1.01         |
| LMU            | 1.00        | 1.00        | 1.01         | 1.02         |
| CSIC           | 1.02        | 1.01        | 1.04         | 1.02         |
| Lapse rate     | 1.01        | 1.00        | 1.02         | 1.01         |
| US standard atmosphere | 1.03 | 1.02 | 1.07 | 1.04 |
Figure A7. Ratios of the O₄ AMFs (a, b) and O₄ dAMFs (c, d) derived for aerosol extinction profiles extracted by different groups vs. those for the standard aerosol extinction profiles (MPIC) for both selected days.

Table A5. Average ratios of O₄ (d)AMFs simulated for different aerosol extinction profiles vs. the results for the standard settings (using the MPIC aerosol extinction profiles) for the middle period on each selected day.

| Aerosol profile | AMF ratios | dAMF ratios |
|-----------------|------------|-------------|
| extraction      | 18 June 2013, 8 July 2013, 11:00–14:00 | 18 June 2013, 8 July 2013, 11:00–14:00 |
| INTE            | 1.01       | 1.02        |
| IUP-B 150 m     | 0.99       | 0.98        |
| IUP-B 300 m     | 0.99       | 1.01        |
| LMU             | 1.00       | 0.99        |

Figure A8. Ratios of the O₄ AMFs (a, b) and O₄ dAMFs (c, d) derived for different extrapolations of the aerosol extinction profiles below 180 m vs. those for the standard settings (linearly extrapolated profiles) for both selected days.
Table A6. Average ratios of O$_4$ (d)AMFs simulated for aerosol extinction profiles with different extrapolations below 180 m vs. the results for the standard settings (linear extrapolation) for the middle period on each selected day.

| Extrapolation below 180 m | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 | AMF ratios | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 | dAMF ratios |
|--------------------------|---------------------------|--------------------------|------------|---------------------------|--------------------------|------------|
| Constant extinction     | 1.02                      | 1.01                     | 1.04       | 1.02                      |                           |            |
| Double slope             | 1.00                      | 0.99                     | 0.99       | 0.98                      |                           |            |

Figure A9. Ratios of the O$_4$ AMFs (a, b) and O$_4$ dAMFs (c, d) derived for different aerosol single-scattering albedos vs. those for the standard settings (single-scattering albedo of 0.95) for both selected days.

Table A7. Average ratios of O$_4$ (d)AMFs simulated for different aerosol single-scattering albedos (SSAs) vs. the results for the standard settings (single-scattering albedo of 0.95) for the middle period on each selected day.

| Single scattering albedo | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 | AMF ratios | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 | dAMF ratios |
|--------------------------|---------------------------|--------------------------|------------|---------------------------|--------------------------|------------|
| 0.9                      | 0.99                      | 0.99                     | 0.99       | 0.99                      |                           |            |
| 1.0                      | 1.03                      | 1.01                     | 1.03       | 1.01                      |                           |            |
Figure A10. Ratios of the $O_4$ AMFs (a, b) and $O_4$ dAMFs (c, d) derived for different aerosol phase functions (HG parameterisation with different asymmetry parameters) vs. those for the standard settings (asymmetry parameter of 0.68) for both selected days.

Table A8. Average ratios of $O_4$ (d)AMFs simulated for different aerosol phase functions (HG parameterisation with different asymmetry parameters (AP) vs. the results for the standard settings (asymmetry parameter of 0.68) for the middle period on each selected day.

| Asymmetry parameter | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 | dAMF ratios |
|---------------------|---------------------------|--------------------------|-------------|
| 0.6                 | 0.98                      | 0.98                     | 0.94        |
| 0.75                | 1.03                      | 1.03                     | 1.08        |

Figure A11. Ratios of the $O_4$ AMFs (a, b) and $O_4$ dAMFs (c, d) simulated by INТА and IUP Bremen and MPIC (SCIATRAN) for phase functions derived from the sun photometer measurements vs. those simulated by MPIC using the Henyey–Greenstein phase function for an asymmetry parameter of 0.68 for both selected days.
Table A9. Average ratios of O₄ (d)AMFs simulated by INTA and IUP Bremen and MPIC (SCIATRAN) for phase functions derived from the sun photometer measurements vs. those simulated by MPIC using the Henyey–Greenstein phase function for an asymmetry parameter of 0.68 for the middle period on each selected day.

| Group (RTM)                | AMF ratios | dAMF ratios |
|----------------------------|------------|-------------|
|                            | 18 June 2013, 11:00–14:00 | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 | 8 July 2013, 07:00–11:00 |
| INTA (LIDORT)              | 1.03       | 1.00        | 1.09            | 1.02             |
| IUP Bremen (SCIATRAN)      | 1.03       | 0.99        | 1.08            | 0.99             |
| MPIC (SCIATRAN)            | 0.97       | 0.98        | 0.95            | 0.95             |

Figure A12. Ratios of the O₄ AMFs (a, b) and O₄ dAMFs (c, d) for different surface albedos vs. those for an albedo of 5 % for both selected days.

Table A10. Average ratios of O₄ (d)AMFs for different surface albedos vs. those for an albedo of 5 % for the middle period on each selected day.

| Surface albedo | AMF ratios | dAMF ratios |
|----------------|------------|-------------|
|                | 18 June 2013, 11:00–14:00 | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 | 8 July 2013, 07:00–11:00 |
| 3 %            | 1.00       | 1.00        | 1.02            | 1.00             |
| 10 %           | 1.02       | 1.01        | 1.00            | 0.99             |
Figure A13. Ratios of the O$_4$ AMFs (a, b) and O$_4$ dAMFs (c, d) simulated by different groups using different radiative transfer models vs. those for the MPIC simulations using McArtim for both selected days.

Table A11. Average ratios of O$_4$ (d)AMFs simulated by different groups using different radiative transfer models vs. those for the MPIC simulations using McArtim for the middle period on each selected day.

| Group (RTM)       | AMF ratios | dAMF ratios |
|-------------------|------------|-------------|
|                   | 18 June 2013, 8 July 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 | 18 June 2013, 8 July 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 |
| CMA (McArtim)     | 1.01       | 1.00        | 1.02       | 1.00        |
| IUP Bremen (SCIATRAN) | 1.02       | 1.01        | 1.04       | 1.03        |
| INTA (LIDORT)     | 1.02       | 1.01        | 1.05       | 1.03        |
| MPIC (SCIATRAN)   | 0.99       | 1.00        | 0.99       | 1.00        |

Figure A14. Ratios of the O$_4$ (d)AMFs considering polarisation vs. those without considering polarisation for both selected days.

Table A12. Average ratios of O$_4$ (d)AMFs considering polarisation vs. those without considering polarisation for the middle period on each selected day.

|                   | AMF ratios | dAMF ratios |
|-------------------|------------|-------------|
|                   | 18 June 2013, 8 July 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 | 18 June 2013, 8 July 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 |
| Considering polarisation | 1.00       | 1.00        | 1.00       | 1.01        |
Table A13. Average ratios of O\textsubscript{4} (d)AMFs derived from synthetic spectra vs. those obtained from radiative transfer simulations at 360 nm for the middle period on each selected day.

| Temperature dependence and noise | AMF ratios | dAMF ratios |
|---------------------------------|------------|-------------|
| 18 June 2013, 8 July 2013, 11:00–14:00 | 1.01 | 1.02 |
| 18 June 2013, 8 July 2013, 07:00–11:00 | 1.00 | 1.00 |

18 June 2013

(a) Measured spectra

(b) Synthetic spectra

8 July 2013

Figure A15. Ratios of the O\textsubscript{4} (d)AMFs derived for different fit windows vs. those for the standard fit window (352–387 nm) for both selected days (a: results for spectra measured by the MPIC instrument; b: results for synthetic spectra when taking into account the temperature dependence of the O\textsubscript{4} cross section).
Table A14. Average ratios of $O_4$ (d)AMFs derived for different fit windows vs. those for the standard fit window (352–387 nm) for the middle period of each selected day (top: results for spectra measured by the MPIC instrument; bottom: results for synthetic spectra when taking into account the temperature dependence of the $O_4$ cross section).

| Spectral range | AMF ratios | dAMF ratios |
|----------------|------------|-------------|
|                | 18 June 2013, 8 July 2013, 11:00–14:00 | 18 June 2013, 8 July 2013, 07:00–11:00 |
| Measured spectra | | |
| 335–374 nm | 0.93 | 0.88 |
| 345–374 nm | 0.98 | 0.99 |
| Synthetic spectra | | |
| 335–374 nm | 0.98 | 0.95 |
| 345–374 nm | 0.99 | 0.98 |

Figure A16. Ratios of the $O_4$ (d)AMFs derived for different polynomials vs. those for the standard analysis (polynomial degree 5) for both selected days (a: results for spectra measured by the MPIC instrument; b: results for synthetic spectra when taking into account the temperature dependence of the $O_4$ cross section).
Table A15. Average ratios of O$_4$ (d)AMFs derived for different polynomials vs. those for the standard analysis (polynomial degree 5) for the middle periods on each selected day (top: results for spectra measured by the MPIC instrument; bottom: results for synthetic spectra when taking into account the temperature dependence of the O$_4$ cross section).

| Degree of polynomial | AMF ratios | dAMF ratios |
|----------------------|------------|-------------|
|                      | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 |
| Measured spectra     |            |             |                        |                       |
| 4                    | 1.04       | 1.02        | 1.06                    | 1.03                   |
| 3                    | 1.03       | 1.03        | 1.06                    | 1.03                   |
| Synthetic spectra    |            |             |                        |                       |
| 4                    | 1.00       | 1.00        | 1.00                    | 1.00                   |
| 3                    | 1.02       | 1.01        | 1.03                    | 1.01                   |

Figure A17. Ratios of the O$_4$ (d)AMFs derived for different intensity offsets vs. those for the standard analysis (intensity offset of degree 2) for both selected days (a: results for spectra measured by the MPIC instrument; b: results for synthetic spectra when taking into account the temperature dependence of the O$_4$ cross section).
Table A16. Average ratios of O$_4$ (d)AMFs derived for different intensity offsets vs. those for the standard analysis (intensity offset of degree 2) for the middle period on each selected day (top: results for spectra measured by the MPIC instrument; bottom: results for synthetic spectra when taking into account the temperature dependence of the O$_4$ cross section).

| AMF ratios | dAMF ratios |
|------------|-------------|
| Intensity offset | 18 June 2013, 8 July 2013, 11:00–14:00 | 07:00–11:00 | 18 June 2013, 8 July 2013, 07:00–11:00 |
| Measured spectra | | | |
| Linear | 1.04 | 1.03 | 1.11 | 1.05 |
| Constant | 1.05 | 1.03 | 1.11 | 1.04 |
| No offset | 1.05 | 1.05 | 1.16 | 1.07 |
| Synthetic spectra | | | |
| Linear | 1.01 | 1.01 | 1.03 | 1.02 |
| Constant | 1.02 | 1.01 | 1.03 | 1.02 |
| No offset | 1.02 | 1.01 | 1.03 | 1.02 |

Figure A18. Ratios of the O$_4$ (d)AMFs derived for the analysis with only one Ring spectrum vs. those for the standard analysis (using two Ring spectra) for both selected days (a: results for spectra measured by the MPIC instrument; b: results for synthetic spectra when taking into account the temperature dependence of the O$_4$ cross section).
Table A17. Average ratios of O₄ (d)AMFs derived for the analysis with only one Ring spectrum vs. those for the standard analysis (using two Ring spectra) for the middle period on each selected day (top: results for spectra measured by the MPIC instrument; bottom: results for synthetic spectra when taking into account the temperature dependence of the O₄ cross section).

| AMF ratios | dAMF ratios |
|------------|-------------|
| Ring correction | | |
| Measured spectra | | |
| Only one Ring spectrum | 1.02 | 0.99 |
| Synthetic spectra | | |
| Only one Ring spectrum | 1.01 | 1.01 |

Figure A19. Ratios of the O₄ (d)AMFs derived for the analysis with a second NO₂ cross section (for 220 K) vs. those for the standard analysis (only NO₂ cross section for 294 K) for both selected days (a: results for spectra measured by the MPIC instrument; b: results for synthetic spectra when taking into account the temperature dependence of the O₄ cross section).

Table A18. Average ratios of O₄ (d)AMFs derived for the analysis with a second NO₂ cross section (for 220 K) vs. those for the standard analysis (only NO₂ cross section for 294 K) for the middle period on each selected day (top: results for spectra measured by the MPIC instrument; bottom: results for synthetic spectra when taking into account the temperature dependence of the O₄ cross section).

| NO₂ cross sections | | |
| AMF ratios | dAMF ratios |
| 294 and 220 K | 1.00 | 1.00 | 1.00 | 1.00 |

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Figure A20. Ratios of the \( \text{O}_4 \) (d)AMFs derived for the analysis with a second \( \text{NO}_2 \) cross section (cross section times wavelength) vs. those for the standard analysis (only one \( \text{NO}_2 \) cross section) for both selected days (a: results for spectra measured by the MPIC instrument; b: results for synthetic spectra when taking into account the temperature dependence of the \( \text{O}_4 \) cross section).

Table A19. Average ratios of \( \text{O}_4 \) (d)AMFs derived for the analysis with a second \( \text{NO}_2 \) cross section (cross section times wavelength) vs. those for the standard analysis (only one \( \text{NO}_2 \) cross section) for the middle period on each selected day (top: results for spectra measured by the MPIC instrument; bottom: results for synthetic spectra when taking into account the temperature dependence of the \( \text{O}_4 \) cross section).

| NO\(_2\) wavelength dependence | AMF ratios | dAMF ratios |
|-------------------------------|------------|-------------|
| 18 June 2013, 11:00–14:00     | 1.00       | 0.99        |
| 8 July 2013, 11:00–14:00      | 1.00       | 1.00        |
| 18 June 2013, 07:00–11:00     | 1.00       | 1.00        |
| 8 July 2013, 07:00–11:00      | 0.98       | 0.99        |
Figure A21. Ratios of the O₄ (d)AMFs derived for the analysis with a second O₄ cross section (accounting for the wavelength dependence) vs. those for the standard analysis (only one O₄ cross section) for both selected days (a: results for spectra measured by the MPIC instrument; b: results for synthetic spectra when taking into account the temperature dependence of the O₄ cross section).

Table A20. Average ratios of O₄ (d)AMFs derived for the analysis with a second O₄ cross section (accounting for the wavelength dependence) vs. those for the standard analysis (only one O₄ cross section) for the middle period on each selected day (top: results for spectra measured by the MPIC instrument; bottom: results for synthetic spectra when taking into account the temperature dependence of the O₄ cross section).

| AMF ratios | dAMF ratios |
|------------|-------------|
| O₄ wavelength dependence | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 |
| Measured spectra | | | | |
| Additional cross section for wavelength dependence | 0.99 | 0.99 | 1.01 | 0.99 |
| Synthetic spectra | | | | |
| Additional cross section for wavelength dependence | 1.00 | 0.99 | 1.00 | 0.99 |
Figure A22. Ratios of the O₄ (d)AMFs derived for the analysis including a H₂O cross section vs. those for the standard analysis (no H₂O cross section) for both selected days (a: results for spectra measured by the MPIC instrument; b: results for synthetic spectra when taking into account the temperature dependence of the O₄ cross section).

Table A21. Average ratios of O₄ (d)AMFs derived for the analysis including a H₂O cross section vs. those for the standard analysis (no H₂O cross section) for the standard analysis (only one O₄ cross section) for the middle period on each selected day (top: results for spectra measured by the MPIC instrument; bottom: results for synthetic spectra when taking into account the temperature dependence of the O₄ cross section).

| H₂O cross section | AMF ratios | dAMF ratios |
|-------------------|------------|-------------|
| H₂O cross section included | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 |
| Measured spectra | 1.00 | 1.00 | 1.01 | 1.01 |
| Synthetic spectra | 0.99 | 1.00 | 0.99 | 0.99 |
(a) Measured spectra

(b) Synthetic spectra

Figure A23. Ratios of the O₄ (d)AMFs derived for the analysis including a HCHO cross section vs. those for the standard analysis (no HCHO cross section) for both selected days (a: results for spectra measured by the MPIC instrument; b: results for synthetic spectra when taking into account the temperature dependence of the O₄ cross section).

Table A22. Average ratios of O₄ (d)AMFs derived for the analysis including a HCHO cross section vs. those for the standard analysis (no HCHO cross section) (only one O₄ cross section) for the middle period on each selected day (top: results for spectra measured by the MPIC instrument; bottom: results for synthetic spectra when taking into account the temperature dependence of the O₄ cross section).

| HCHO cross section | AMF ratios | dAMF ratios |
|--------------------|------------|-------------|
| Measured spectra   |            |             |
| HCHO cross section included | 1.00 | 1.00 | 0.96 | 0.98 |
| Synthetic spectra  |            |             |
| HCHO cross section included | 0.97 | 0.99 | 0.94 | 0.97 |
Figure A24. Ratios of the O₄ (d)AMFs derived for the analyses using different O₄ cross sections vs. those for the standard analysis (using the Thalman and Volkamer cross section) for both selected days (a: results for spectra measured by the MPIC instrument; b: results for synthetic spectra when taking into account the temperature dependence of the O₄ cross section).
Table A23. Average ratios of O₄ (d)AMFs derived for the analyses using different O₄ cross section vs. those for the standard analysis (using the Thalman and Volkamer cross section) for the standard analysis (only one O₄ cross section) for the middle period on each selected day (top: results for spectra measured by the MPIC instrument; bottom: results for synthetic spectra when taking into account the temperature dependence of the O₄ cross section).

| O₄ cross section | AMF ratios | dAMF ratios |
|-----------------|------------|-------------|
|                 |            |             |
| 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 |
| Measured spectra |            |             |
| Hermans         | 0.98       | 0.97        | 0.97 |
| Greenblatt      | 1.03       | 1.07        | 1.08 |
| Greenblatt shifted | 1.01       | 1.03        | 1.03 |
| Synthetic spectra |            |             |
| Hermans         | 0.97       | 0.94        | 0.94 |
| Greenblatt      | 1.03       | 1.07        | 1.08 |
| Greenblatt shifted | 1.01       | 1.02        | 1.03 |

Figure A25. O₄ differential box AMFs (with 20 m vertical resolution) used for the simulation of the temperature-dependent O₄ absorption spectra. They are averages of radiative transfer simulations for several scenarios. Simulations are performed for a surface albedo of 6%, aerosol profiles with constant extinction between 0 and 1000 m and different AOD (0.1, 0.3, 0.7) and for all combinations of SZA (40, 60°), RAZI (0, 90, 180°) and elevation angles (2 and 3°).
Figure A26. Ratios of the O₄ (d)AMFs derived for O₄ cross sections at different temperatures (either 203 K or both 203 and 293 K) vs. those for the standard analysis (using the O₄ cross section for 293 K) for both selected days (a: results for spectra measured by the MPIC instrument; b: results for synthetic spectra when taking into account the temperature dependence of the O₄ cross section).
Table A24. Average ratios of O₄ (d)AMFs derived from O₄ cross sections at different temperatures (either 203 K or both 203 and 293 K) vs. those for the standard analysis (using the O₄ cross section for 293 K) for the middle period on each selected day (top: results for spectra measured by the MPIC instrument; bottom: results for synthetic spectra when taking into account the temperature dependence of the O₄ cross section). For the simultaneous fit of both temperatures the results for the spectral range 345–374 nm (one O₄ absorption band) are also included.

| O₄ cross sections | AMF ratios | dAMF ratios |
|-------------------|------------|-------------|
|                   | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 |
| Measured spectra  |            |             |                         |                         |
| 203 K             | 0.85       | 0.82        | 0.70                    | 0.70                    |
| 203 and 293 K     | 1.00       | 1.02        | 1.04                    | 1.01                    |
| 203 and 293 K (345–374 nm) | 0.91 | 1.04 | 0.95 | 1.02 |
| Synthetic spectra |            |             |                         |                         |
| 203 K             | 0.86       | 0.84        | 0.70                    | 0.69                    |
| 203 and 293 K     | 0.91       | 0.94        | 0.82                    | 0.89                    |
| 203 and 293 K (345–374 nm) | 0.99 | 1.00 | 0.99 | 1.00 |

Figure A27. (a) Comparison of the O₄ cross sections from Thalman and Volkamer (2013) for different temperatures. The cross sections are divided by the maximum values at 360 nm. After this normalisation, the resulting values at 380 nm fall into two groups (high values for 203 and 233 K, low values for 253, 273 and 293 K). (b) Ratios of the peaks of the O₄ cross section at 360 and 380 nm as a function of temperature (red points). The black curve is a fitted low-order polynomial.
Figure A28. Ratios of the retrieved O₄ dSCDs for 203 and 293 K as well as the derived effective temperatures for the analyses with both cross sections included.
Table A25. (a) Average ratios of O$_4$ (d)AMFs derived from the analysis of MPIC spectra by different groups vs. the analysis of MPIC spectra by MPIC (standard analysis). (b) Average ratios of O$_4$ (d)AMFs derived from spectra of other groups analysed by MPIC vs. the analysis of MPIC spectra by MPIC (using the same analysis settings and spectral range: 335–374 nm). (c) Average ratios of O$_4$ (d)AMFs derived from spectra of other groups analysed by the same groups using individual analysis settings vs. the analysis of MPIC spectra by MPIC (standard analysis).

| Measurements and analysis | AMF ratios | dAMF ratios |
|---------------------------|------------|-------------|
|                           | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 |
|                           | 18 June 2013, 11:00–14:00 | 8 July 2013, 07:00–11:00 |
| (a) MPIC spectra analysed by other groups |            |              |
| BIRA                      | 0.96       | 0.95         |
| IUP-B                     | 1.03       | 1.05         |
| INTA                      | 1.02       | 1.05         |
| CMA                       | 0.97       | 0.98         |
| CSIC                      | 0.94       | 0.95         |
| (b) Other spectra analysed by MPIC (335–374 nm) |            |              |
| BIRA                      | 0.98       | 0.89         |
| IUP-B                     | 1.05       | 1.07         |
| IUP-HD                    | 0.97       | 1.00         |
| (c) Other spectra analysed by the same groups |            |              |
| BIRA                      | 0.94       | 0.91         |
| IUP-B                     | 0.95       | 0.88         |
| IUP-HD                    | 1.01       | 1.04         |
A5 Extraction of aerosol extinction profiles

In this section, the procedure for the extraction of aerosol extinction profiles is described. The aerosol profiles are derived from the ceilometer measurements (yielding the profile information) in combination with the sun photometer measurements (yielding the vertically integrated aerosol extinction, the AOD).

The raw ceilometer data consist of range-corrected backscatter profiles averaged over 15 min. The profiles range from the surface to an altitude of 15 360 m with a height resolution of 15 m. Here it is important to note that, due to limited overlap of the outgoing laser beam and the field of view of the telescope, no profile data are available below 180 m. The ceilometer profiles (hourly averages) are shown in Fig. A29 for both selected days.

The AERONET sun photometer data provide the AOD at different wavelengths (340, 360, 440, 500, 675, 870 and 1020 nm) at time intervals of 2–25 min if the direct sun is visible.

To determine profiles of aerosol extinction from the ceilometer backscatter data, several processing steps have to be performed. They are described in the subsections below. Note that in this section the individual steps are described according to the MPIC procedure. The extracted profiles from other groups differ slightly compared to the results of the MPIC procedure, especially with respect to the altitude above which the extinction was set to zero (see Fig. 9).

A5.1 Smoothing and extrapolating of the ceilometer backscatter profiles

First, the ceilometer data are averaged over several hours to reduce the scatter. For that purpose on both days three time periods are identified, for which the backscatter profile shows relatively small variations. The profiles for these periods are shown in Fig. A29. In addition to the temporal averaging, the profiles are vertically smoothed above 2 km. Above altitudes between 5 and 6 km (depending on the period) the (smoothed) ceilometer backscatter profiles become zero. Thus, the aerosol extinction profiles above these altitudes are set to zero.

Below 180 m above the surface the ceilometer becomes “blind” for the aerosol extinction because of the insufficient overlap between the outgoing laser beam and the field of view of the telescope. Thus, the profiles have to be extrapolated down to the surface. This extrapolation constitutes an important source of uncertainty. To estimate the associated uncertainties, the extrapolation is performed in three different ways:

1. The values below 180 m are set to the value measured at 180 m.
2. The values below 180 m are linearly extrapolated assuming the same slope below 180 m as between 180 and 240 m.
3. The values below 180 m are linearly extrapolated by twice the slope between 180 and 240 m.

A5.2 Scaling of the ceilometer profiles by sun photometer AOD at 1020 nm

The scaling of the ceilometer backscatter profiles by the AOD at 1020 nm is an intermediate step, which is necessary for the correction of the aerosol self-extinction. The average AOD at 1020 nm for the different selected time periods on both days is shown in Table A26. In that table the average values at 380 nm are also shown, which are used for a second scaling (see below).

The backscatter profiles are vertically integrated and then the whole profiles are scaled by the ratio:

\[
\alpha_{i, \text{corr}} = \frac{\alpha_i}{\exp\left(-2 \cdot \sum_{j=0}^{i-1} \alpha_{i, \text{corr}} \cdot (z_j - z_{j-1})\right)}.
\]

Here \(B_{\text{int}}\) indicates the integrated backscatter profile.

Note that the wavelength of the ceilometer measurements (1064 nm) is slightly different from the sun photometer measurements (1020 nm), but the difference of the AOD is negligible (typically < 4%).

A5.3 Correction of the aerosol extinction

The photons received by the ceilometer have undergone atmospheric extinction. Here, Rayleigh scattering can be ignored because of the long wavelength of the ceilometer (optical depth below 2 km is < 0.001). However, while the extinction due to aerosol scattering is also small at these long wavelengths it systematically affects the ceilometer signal and has to be corrected. The extinction correction is performed according to the following formula:

\[
\alpha_{i, \text{corr}} = \frac{\alpha_i}{\exp\left(-2 \cdot \sum_{j=0}^{i-1} \alpha_{i, \text{corr}} \cdot (z_j - z_{j-1})\right)}.
\]

Table A26. Average AOD derived from the sun photometer at 1020 and 360 nm.

| Time                  | AOD 1020 nm | AOD 360 nm |
|-----------------------|-------------|------------|
| 18 Jun 2013, 08:00–11:00 | 0.124       | 0.379      |
| 18 Jun 2013, 11:00–14:00 | 0.122       | 0.367      |
| 18 Jun 2013, 14:00–19:00 | 0.118       | 0.296      |
| 8 Jul 2013, 04:00–07:00   | 0.045       | 0.295      |
| 8 Jul 2013, 07:00–14:00   | 0.053       | 0.333      |
| 8 Jul 2013, 11:00–19:00   | 0.055       | 0.348      |

\(\text{Average of AOD at 340 and 380 nm.}\)
Here $\alpha_i$ represents the uncorrected extinction and $\alpha_{i,\text{corr}}$ represents the corrected extinction at height layer $i$ (with $z_i$ is the lower boundary of that height layer). Equation (A2) has to be subsequently applied to all height layers starting from the surface ($z_0$). Note that the factor of 2 accounts for the extinction along both paths between the instrument and the scattering altitude (upward and downward). The extinction correction is performed at a vertical resolution of 15 m.

After the extinction correction, the profiles are scaled by the corresponding AOD at 360 nm (see Table A26). In Fig. A30 the profiles with and without extinction correction are shown. The extinction correction slightly increases the values at higher altitudes and decreases the values close to the surface. The effect of the extinction correction is larger on 18 June 2013 (up to 12 %).
A5.4 Influence of a changing lidar ratio with altitude

For the extraction of the aerosol profiles described above, a fixed lidar ratio was assumed, which implies that the aerosol properties are independent from altitude. However, this is a rather strong assumption, because it can be expected that the aerosol properties (e.g., the size) change with altitude. With the available limited information, it is impossible to derive detailed information about the altitude dependence of the aerosol properties, but it can be quantified how representative the ceilometer measurements at 1064 nm are for the aerosol extinction profiles at 360 nm. For these investigations we again focus on the middle periods of both selected days. From the AERONET Almucantar observations information on the size distribution for these periods is available (see Fig. A32). On both days two pronounced modes (fine and coarse mode) are found with a much larger coarse-mode fraction on 18 June compared to 8 July (on 18 June the coarse mode is broader and shows two distinct maxima). From the AERONET observations, separate phase functions for the fine and coarse mode, as well as the relative contri-
In the last step the probability of aerosol scattering in the backward direction is considered, because the ceilometer receives scattered light from that direction. For that purpose the ratios of the optical depths are multiplied by the corresponding values of the normalised phase functions at 180° and in this way the relative contributions to the backscattered signals from the coarse mode for both wavelengths and both days are calculated (Table A28). Interestingly, on 8 July the contributions of the coarse mode to the backscattered signal at both wavelengths differ by only about 10 %. In contrast, on 18 June the difference is much larger.

For 8 July, the results can be interpreted in the following way: at 360 nm the aerosol profiles extracted as described above overestimate the contribution from the coarse mode by about 10 %. To estimate the effect of this overestimation we construct modified aerosol extinction profiles, in which 10 % of the total AOD is relocated. Since we expect that the coarse-mode aerosols are usually located at low altitude, we construct four different modified profiles (see Fig. A33) with different altitudes (1.5, 1, 0.75, or 0.5 km), below which 10 % of the aerosol extinction is relocated to altitudes above (assuming that the coarse-mode aerosol is only located below these altitudes). Of course, such a sharp boundary is not very realistic, but it allows the overall effect of the relocation to be quantified. We selected the aerosol profile for 8 July extracted by INTA, which reached up to 7 km (see Fig. 9). It should be noted that if 10 % of the total AOD is relocated from the lowest layer to only the uppermost layer no further enhancement of the O₄ dAMF is found (see Appendix A6).

For all modified profiles, a systematic increase in the O₄ (d)AMFs compared to those for the standard settings is found. For the O₄ dAMFs this increase can be up to 18 % (see Table A29. From the comparison of the elevation dependence of the measured and simulated O₄ dAMFs (see Fig. A33), we conclude that the aerosol profile with the coarse-mode aerosol below 0.75 km is probably the most realistic one. The main conclusion from this section is that the dAMF for 8 July derived from the standard settings probably underestimates the true dAMF by about 17 ± 5 %.

For 18 June we did not perform similarly detailed calculations, because on that day the uncertainties of the aerosol extinction profile caused by the missing sensitivity of the ceilometer below 180 m are much larger than on 8 July. On 18 June the magnitude of the relocation of the aerosol extinction between different altitudes would also be much larger than on 8 July.

A6 Influence of elevated aerosol layers on the O₄ (d)AMF

Ortega et al. (2016) showed that for their measurements the consideration of elevated aerosol layers (between about 3 and 5 km) is essential to bring measured and simulated O₄ (d)AMFs into agreement. They also used lidar measurements at similar wavelengths as the MAX-DOAS observations. In
Table A27. Contributions of the coarse mode to the total AOD at different wavelengths derived from AERONET observations. The relative contributions are calculated assuming that the AOD of the coarse mode at 500 nm (0.093 and 0.010 on 18 June and 8 July, respectively) does not depend on wavelength.

| Date             | Total AOD 360 nm | Total AOD 500 nm | Total AOD 1064 nm | Relative contribution of coarse mode 360 nm | Relative contribution of coarse mode 500 nm | Relative contribution of coarse mode 1064 nm |
|------------------|------------------|------------------|-------------------|--------------------------------------------|--------------------------------------------|--------------------------------------------|
| 18 June, 11:00–14:00 | 0.37             | 0.242            | 0.119             | 24.9 %                                     | 38.7 %                                     | 77.7 %                                     |
| 8 July, 07:00–11:00 | 0.33             | 0.207            | 0.0535            | 3.0 %                                      | 4.8 %                                      | 18.7 %                                     |

* This value was extrapolated from the measurements at 675 and 1020 nm.

Table A28. Ratios of phase functions (coarse/fine) in exactly backward direction and the relative contribution of coarse mode to the backscattered signal at both wavelengths.

| Date             | Ratio phase function at 360 nm | Ratio phase function at 1064 nm | Relative contribution of coarse mode at 360 nm | Relative contribution of coarse mode at 1064 nm |
|------------------|---------------------------------|---------------------------------|-----------------------------------------------|-----------------------------------------------|
| 18 June, 11:00–14:00 | 1.13                            | 0.61                            | 27.3 %                                       | 68.0 %                                       |
| 8 July, 07:00–11:00 | 2.7                             | 0.99                            | 7.8 %                                        | 18.3 %                                       |

From these results it can be concluded that for a relocation of about 27% almost perfect agreement with the measurements is found (see Fig. A34). For such an aerosol profile simulations and measurements could be brought into agreement without a scaling factor. However, such a large redistribution is not supported by the AERONET inversion products (see Appendix A5). It should also be noted that for such a profile, about 73% of the total AOD would be located above about 1.7 km. Moreover, for such an aerosol profile it is found that the simulated O_4 AMFs for 90° elevation systematically underestimate the measured O_4 AMFs at high SZA by about 15% (see Fig. A34), whereas much better agreement is found for the standard settings. The underestimation of the O_4 AMFs for 90° elevation is caused by the high aerosol amount at high altitudes, which increases the scattering altitude of the solar photons observed at 90° elevation. A similar effect could be caused by cirrus clouds, but on the selected days there are no indications of such clouds in the ceilometer data.
Figure A33. (a) Modified aerosol profiles for 8 July assuming that the coarse-mode aerosol is only located in the lowest part of the atmosphere. (b) Ratios of the (d)AMFs calculated for the modified profiles compared to the dAMFs for the standard settings. With decreasing layer height the (d)AMFs increase systematically, because the aerosol extinction close to the surface decreases. (c) Comparison of the measured elevation dependence of the O₄ dAMFs for the period 07:00–11:00 on 8 July and simulation results for the different profiles.

Table A29. Ratios of the (d)AMFs for the modified profiles vs. those of the standard settings.

|                | Original INTA | Coarse mode below 1.5 km | Coarse mode below 1 km | Coarse mode below 0.75 km | Coarse mode below 0.5 km |
|----------------|---------------|--------------------------|------------------------|---------------------------|--------------------------|
| AMF            | 1.02          | 1.04                     | 1.05                   | 1.06                      | 1.08                     |
| dAMF           | 1.04          | 1.09                     | 1.13                   | 1.17                      | 1.18                     |

Table A30. Selection of different aerosol layers on 8 July (07:00–11:00).

| Layer      | AOD  | Relative contribution to total AOD |
|------------|------|-----------------------------------|
| 0–1.68 km  | 0.186 | 55.4 %                           |
| 1.68–4.9 km| 0.116 | 34.5 %                           |
| 4.9–7 km   | 0.035 | 10.4 %                           |
Figure A34. (a) Aerosol profiles used for the simulations (see text). (b) Ratios of the $O_4$ (d)AMFs simulated for the modified profiles vs. those of the original profile. (c, d) Comparison of the measured diurnal variation (SZA dependence) for 90° elevation (c) and the elevation dependence of the $O_4$ dAMFs for the period 07:00–11:00 on 8 July (d).

Table A31. Ratios of (d)AMFs for 8 July 2013 for the modified profiles with respect to the original profile.

|          | AMF  | dAMF |
|----------|------|------|
| Low      | 1.00 | 0.94 |
| +40 %    | 1.06 | 1.08 |
| Middle   | 1.04 | 1.04 |
| +40 %    | 1.07 | 1.17 |
| Top      | 1.12 | 1.31 |
| 10 % bottom to top | 1.20 | 1.48 |
| 25 % bottom to top |     |     |
| 30 % bottom to top |     |     |

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