Geolectric field measurement, modelling and validation during geomagnetic storms in the UK

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Abstract—Significant geolectric fields are produced by the interaction of rapidly varying magnetic fields with the conductive Earth, particularly during intense geomagnetic activity. Though usually harmless, large or sustained geolectric fields can damage grounded infrastructure such as high-voltage transformers and pipelines via geomagnetically induced currents (GICs). A key aspect of understanding the effects of space weather on grounded infrastructure is through the spatial and temporal variation of the geolectric field. Globally, there are few long-term monitoring sites of the geolectric field, so in 2012 measurements of the horizontal surface field were started at Lerwick, Eskdalemuir and Hartland observatories in the UK. Between 2012 and 2020, the maximum value of the geolectric field observed was around 1 V/km in Lerwick, 0.5 V/km in Eskdalemuir and 0.1 V/km in Hartland during the March 2015 storm. These long-term observations also allow comparisons with models of the geolectric field to be made. We use the measurements to compute magnetotelluric impedance transfer functions at each observatory for periods from 20 to 30,000 s. These are then used to predict the geolectric field at the observatory sites during selected storm times that match the recorded fields very well (correlation around 0.9). We also compute geolectric field values from a thin-sheet model of Britain, accounting for the diverse geological and bathymetric island setting. We find the thin-sheet model captures the peak and phase of the band-passed geolectric field reasonably well, with linear correlation of around 0.4 in general. From these two modelling approaches, we generate geolectric field values for historic storms (March 1989 and October 2003) and find the estimates of past peak geolectric fields of up to 1.75 V/km in Eskdalemuir. However, evidence from high voltage transformer GIC measurements during these storms suggests these estimates are likely to represent an underestimate of the true value.

Keywords: geolectric field / magnetotellurics / thin-sheet model / conductivity / geomagnetically induced currents

1 Introduction

During severe space weather events, the Earth’s magnetic field can change rapidly with large variations in the order of thousands of nT (e.g. Hapgood, 2019). The time variations of the externally-produced magnetic field induce electric fields in the conductive ground, whose magnitude and spatial scale depend on the underlying electrical conductivity structure. For long period variations (hundreds to thousands of seconds) in resistive geology, the skin-depth is large (10–100 km) and the magnetic field generates a large geolectric field. Short period variations (tens of seconds) of the magnetic field in a conductive subsurface have shallow skin depths (0.1–1 km) and do not produce strong geolectric fields (e.g. Simpson & Bahr, 2005).

Lateral contrast in conductivity caused by complex geologic, topographic and bathymetric variations can contribute to strong geolectric fields over large areas, which can be up to several tens of V/km (Myllys et al., 2014; Love et al., 2018) posing a hazard to modern technology. With widespread adoption of low-resistance grounded infrastructure such as high voltage (HV) power networks induced geolectric fields can equalize through the earthing points of these conductors. These quasi-steady DC currents are called geomagnetically induced currents (GICs) and, though small in comparison to the load carried, are a threat to the safe and optimal operation of HV transformers (Boteler, 2006; Pulkkinen et al., 2012). The most widely cited example of GIC damage is the collapse of a Québec-Hydro network in March 1989 (Bolduc, 2002; Boteler, 2019). Recent estimates of the cost of a similar widespread power outage suggest losses on the order of tens of billions of US dollars per day in advanced economies (e.g. Schulte in den Bäumen et al., 2014; Oughton et al., 2018).

Over the past two decades, a large effort has been directed towards understanding the risk posed to power networks across...
the world (Mac Manus et al., 2017; Rosenqvist & Hall, 2019; Sokolova et al., 2019). GICs are a function of the induced geoelectric field coupled to the resistance and topology parameters of the affected power grid (e.g. Albertson et al., 1981). Modelling the response of a power grid to a uniform input geoelectric field is generally well-understood and many GIC analyses begin at this point (Horton et al., 2012; Caraballo et al., 2020). This simple field structure has often been adopted by industry within worst case scenarios and real-time analysis software (e.g. Femberg, 2012; North-American Electric Reliability Corporation, 2016). However, research over the past decade has shown that this assumption is too simplistic and will cause a poor estimate of GIC during even modest storms (Beggan et al., 2013; Viljanen & Pirjola, 2017; Blake et al., 2018; Love et al., 2018; Sun & Balch, 2019). Hence, both the spatial and temporal pattern of the magnetic field and the underlying conductivity structure must be accounted for in order to produce realistic geoelectric field models over a wide region (Lucas et al., 2020).

Locally, natural variations in the geoelectric and magnetic field can be measured using three or more non-polarizable electrodes to record the voltage in an east–west and north–south direction in conjunction with a three-axis magnetometer. This is the basis of the magnetotelluric (MT) method (Cagniard, 1953; Watt, 1982) which derives a frequency-dependent stationary transfer function between the magnetic and electric fields, the impedance tensor, using the assumption that the inducing magnetic field is spatially uniform. Typically, MT sites are occupied from a few days to a couple of months allowing for a transfer function with periods between 0.01 s and around 100,000 s to be computed (Chave & Jones, 2012). The impedance tensor can then be used to estimate the induced geoelectric field at any other time when only magnetic field recordings or models are available.

Longer term measurements of the geoelectric field are rarer and are only available at a few locations around the world including the UK, Japan (Fujii et al., 2015), Hungary (Kis et al., 2007) and the USA (Blum et al., 2017). The earliest known long-term measurements in the UK are from the Greenwich observatory in London where geoelectric field measurements were made between 1868 and 1895, before noise from the recently-introduced DC electric trains prevented the natural signal from being observed. The Greenwich system used four copper grounding plates separated by approximately 5 km with wiring running along the (pre-electrified) railway lines around London. The geoelectric field was measured by the deflection of an iron needle placed between two coils sited in the observation hut, subsequently recorded onto photographic paper. Plots of the original geoelectric field measurements are available in the observatory yearbooks, for example, but are usually un-scaled (though see Preece, 1882 who reported a current of 3.3 A).

The Japanese and Hungarian measurements have been ongoing for many decades, since the International Geophysical Year (1957) in the case of Hungary and even earlier for Kakioka Observatory (beginning in 1932). Measurement campaigns in the USA have been sporadic in the past century but continuous monitoring was restarted in 2016 at Boulder Observatory. Since 2012, the British Geological Survey (BGS) have collected geoelectric field measurements at their three UK observatories at a cadence of 10 Hz, transmitting them in real-time to the data centre in Edinburgh. The three BGS observatories are located in the far north on the Shetland Islands (Lerwick), southern Scotland (Eskdalemuir) and southwest England (Hartland), shown in Figure 1a. With these exceptions, long-term real-time geoelectric field measurements are extremely limited across the globe.

The paucity of widespread measurements of the geoelectric field elsewhere means it must instead be modelled. Kelbert (2020) provides a review on the contemporary state-of-the-art in GIC and geoelectric field modelling. There are three main approaches for calculating the geoelectric field from measured magnetic field variations: (a) homogeneous fields from half-space or 1D conductivity models (e.g. Boteler & Pirjola, 1998), (b) 2D maps of the electric field at the surface created from models of bulk lithological properties, MT surveys or from airborne measurements in a thin-sheet or multi-sheet model (e.g. Thomson et al., 2005; Ivannikova et al., 2018) or (c) full 3D conductivity estimates of the electric field using finite element analysis derived from inversion of a large number of measurements or synthetic models (e.g. Pokhrel et al., 2018; Rosenqvist & Hall, 2019). These three approaches can be considered to represent the end-members in the trade-off between accuracy, speed of computation and spatial applicability. For example, approach (a) is fast and accurate to compute but is only representative at a single location, while approach (c) is accurate and can reproduce the geoelectric field across a large region but requires large resources to compute. At present, approach (b) offers a compromise between the three factors, offering lower accuracy but capturing a wide area with reasonably quick computation times.

As well as the above trade-offs, differing levels of effort are required to construct the models. In the case of approach (a), 1D models, often from magnetotelluric measurements must be made across a large region (or country) which can take many years to complete (Schultz et al., 2006–2018) and significant resources, though the advantage is that the model constantly improves with more data. Approach (c) requires significant effort to create a large-scale 3D model (e.g. Robertson et al., 2020), which may be made from information gathered from MT surveys and other sources, but may have larger uncertainties in regions without ground measurements. Finally, approach (b) is based on incomplete knowledge of lithological and deep crustal conductivity acquired from geological surveys but is feasible to construct from readily-available information (see Beamish, 2013, and references therein). While all these approaches offer plausible models of the geoelectric field (within a narrow period range) based on ground conductivity, validating them across a large region is more difficult.

Progress in recent years has focused on making better use of existing data. Marshall et al. (2019) examine some of the different methods of combining 1D or 3D conductivity models of approach (a), as do Kelbert et al. (2017). Over the past decade, we have used the thin-sheet approach to model the geoelectric response to increased geomagnetic activity due to space weather in the UK. The thin-sheet model is based on the approach by Vasseur & Weidelt (1977) as modified by Beamish et al. (2002) and McKay (2003). The model consists of 10 km grid cells representing the conductance of the 2D surficial lithology (to a depth of 3 km) with a series of 1D conductivity models at depth to represent the six geological terranes beneath the British Isles. The thin-sheet model code has been used to study the GIC risk in the UK (Beggan et al., 2013;
Beggan, 2015; Kelly et al., 2017), as well as in Austria (Bailey et al., 2018) and New Zealand (Divett et al., 2020). However, thin-sheet models are known to have limitations and provide a general approximation of the true geoelectric field rather than a highly accurate model.

In the following sections, we focus on three main aspects of recent BGS work in geoelectric field research to provide an overview of our present capabilities. Firstly, we describe the three UK geoelectric observatories and give examples of their measurements (Sect. 2). We use the long-term geoelectric and magnetic field measurements to compute MT transfer functions for the observatories in Sections 3 and in Section 4, we describe the thin-sheet method in detail. In Section 5, we compare the geoelectric field computed by the MT transfer functions and output by the thin-sheet model with the independent measurements made at the observatories for a number of geomagnetic storms. Finally, we use both the MT impedance functions and the thin-sheet model to estimate the geoelectric field induced during the two largest storms of the digital era (March 1989 and October 2003) in Section 6. We discuss the results in Section 7 before making our conclusions.

2 Measuring the geoelectric field

For long-term measurements of the geoelectric field, the voltage between two points in the ground is measured using a pair of non-polarising electrodes to minimise self-potential that would otherwise appear as noise in the recording of differential voltage data (and therefore contaminate the signal of interest). At each UK observatory a similar (though not identical) set of sensors and recording equipment are used. The electrodes are of the LEMI-701 type, manufactured at the Lviv Centre of Institute for Space Research, Ukraine (https://lemisensors.com/). These were chosen for their low noise and long-term stability. The LEMI-701 electrodes are set into a copper and copper-sulphate solution (Cu-CuSO₄), as shown in Figure 1b. At the observatories, two pairs of electrodes are installed in small hand-dug pits at least 0.5 m deep and set in a clay-CuSO₄ mix aligned in geographical North–South and East–West directions, with a dipole length of between 66 and 100 m.

At the northernmost observatory, Lerwick, the observatory lies around 4 km southwest of a small town on a short peninsula surrounded by the sea. The terrain is generally wet, on a slight incline to the south, and is bounded by a small freshwater lake at the southern edge. The North–South probes are separated by 99 m and the East–West probes are 91 m apart. Through an analogue to digital converter (ADC) with bespoke pre-amplifiers, a Guralp data logger collects and stores the data before it is sent in real-time across the internet to the BGS office in Edinburgh. The Lerwick system was installed in early 2012.

The Eskdalemuir observatory occupies a quiet rural valley in the southern part of Scotland approximately 35 km from the west coast and 70 km from the east coast. The geoelectric field probes are installed around 400 m from the nearest building in a wet boggy field. The North–South probes are separated by 99 m and the East–West probes are 91 m apart. Through an analogue to digital converter (ADC) with bespoke pre-amplifiers, a Guralp data logger collects and stores the data before it is sent in real-time across the internet to the BGS office in Edinburgh. The Eskdalemuir system began recording in mid-2013.

Hartland observatory lies in the southwest corner of England close to the Bristol Channel. The site is a few hundred metres north of Hartland village on flat, relatively dry and well-drained land. The North–South probes are separated by 69 m and the East–West probes are 76 m apart, shown as blue lines.
in Figure 1c. A similar data collection system to the other observatories exists. The geoelectric field system in Hartland was installed in early 2013.

Data from all three observatories are posted to the BGS website every 10 min and plots showing the past 6 h, the day to date and the past 30 days are available for browsing. Figure 1d shows a stackplot of the north–south component from Hartland for June 2013. There is a clear lunar tidal signal visible (approximately 20 mV/km peak to peak) with a period of 12.42 h. Note that some minor space weather activity is visible at the beginning of Days 1 and 29.

The geoelectric field systems were installed to test whether good quality data could be collected at the existing geomagnetic observatories. Due to the generally challenging environments in the remote locations and the normal decay of the probes, maintaining continuous high-quality measurements has not been possible. Various redesigns of the systems over the years as well as damage from lightning or component failure have caused gaps or poor quality data for analysing longer periods. This is in addition to drifts caused by the degradation of the probes and occasional steps in the data. However, a considerable effort has been made to clean up the dataset where feasible and new instrumentation is planned.

In addition to the range of geomagnetic latitudes, the three observatories lie in very different settings in terms of proximity to the coast, altitude and underlying geology. This gives rise to strong variations in the electric and magnetic environment experienced during space weather events. Due to the relatively quiescent nature of space weather in the approximately eight years of operation to date, the geoelectric field measurements encompass relatively few intense events e.g. the 17 March 2015 and the 7–8 September 2017 storms are two of the larger storms of solar cycle 24.

Figures 2 and 3 show the minute-mean values of the magnetic and geoelectric fields recorded at the three observatories for these dates. The upper panels (a–c) shows the horizontal strength of the magnetic field variation \((H = \sqrt{X^2 + Y^2})\) relative to its quiet time background (in nT) with the variation of the two geoelectric horizontal field components (in mV/km). Note the curves have been offset from each other to show the detail. It can be observed at each site that it is the high frequency variations of the magnetic field that induce the geoelectric field with the long period variations being largely damped. Only Hartland has long-period variations due to the tidally-induced field from high range and rapid flow of seawater in the Bristol Channel.

The bottom panel (d) in both figures shows the measured GIC from a Hall probe installed at Torness 400 kV substation in central Scotland, around 90 km northeast of Eskdalemuir (McKay, 2003). The GIC response of the high voltage power grid can be considered to be a band-pass filtered version of the geoelectric field. Again, it is clear that the short-period variations of the geoelectric field have the strongest influence on measured GIC.

Finally, a storm on the 26 August 2018 is shown in Figure 4. Though a relatively minor storm (G3 on the NOAA geomagnetic storm scale), it coincided with the deployment of the differential magnetometer method (DMM) systems of Hübert et al. (2020) which allowed a comparison of both line and substation GIC to be made. Unfortunately, only a single channel of electric field data at each observatory was in operation due to various technical issues. Note the variation of the magnetic and geoelectric fields are smaller than the 2015 and 2017 storms as were the resultant GICs.

3 Magnetotelluric impedance functions

Using the geoelectric \((E)\) and simultaneous magnetic field \((B)\) measurements at the three observatories we computed the
magnetotelluric impedance tensor \( Z \) at each site (e.g. Wait, 1982). It is defined in the frequency domain as:

\[
E(\omega) = \frac{1}{\mu_0} Z(\omega) \cdot B(\omega)
\]

with \( \mu_0 \) the magnetic permeability and the angular frequency \( \omega \). We chose six months during 2015 of uninterrupted and relatively noise-free time-series from each observatory to derive the impedance in the frequency range of 20–30,000 s using the robust statistical algorithm of Smirnov (2008). \( Z \) is assumed to be temporarily stationary – it represents the underlying electrical conductivity distribution which can be assumed to be constant in the case of the UK. We tested this and derived \( Z \) from different time periods of recordings at the three observatories with almost identical outcomes (within the uncertainties).

Fig. 3. Measurements of the geoelectric field components (North–South & East–West), the variation of the horizontal component \( \mathbf{H} \) of the magnetic field and GIC (in amps) for 7–8 September 2017. (a) Lerwick; (b) Eskdalemuir; (c) Hartland; (d) GIC at Torness substation, East Scotland. Note the magnetic and geoelectric curves are offset from zero.

Fig. 4. Measurements of the geoelectric field component (North–South or East–West), the variation of the horizontal component \( \mathbf{H} \) of the magnetic field and GIC (in amps) for 25–26 August 2018. Only one electric channel at each site was available. (a) Lerwick; (b) Eskdalemuir; (c) Hartland; (d) GIC from Torness substation, East Scotland. Note the magnetic and geoelectric curves are offset from zero.
Figure 5 shows the components of the impedance for periods of 20–30,000 s for each of the three observatories. The transfer functions show the largest response at short periods (20–1000 s) with an approximately exponential decrease (i.e. a linear change in logarithmic scale) with longer periods beyond 1000 s. This is consistent with the observations of the geomagnetic to geoelectric response in Figures 2–4. In general, Hartland has the weakest magnitude response to magnetic field variations, while Lerwick and Eskdalemuir have a stronger response. The differences in the structure of the curves for each component relate primarily to the geology beneath each site, though at longer periods the associated errors become larger too (not shown).

From our observations, during storm times, the geoelectric field estimates from the MT transfer functions tend to underestimate the magnitude of the measured geoelectric field. This can be attributed to a number of causes, as discussed for example in Campanya et al. (2019). Some signal loss can be explained by the limited frequency content (the magnetic field data is sampled at 1 min and the impedance tensor is only derived for 10–30,000 s). Additionally, the plane wave approximation, fundamental for the MT tensor relationship, may not be able to explain all of the signal during geomagnetic storm times (Viljanen et al., 1999; Romano et al., 2014; Simpson & Bahr, 2020). For example, Simpson & Bahr (2021) demonstrate they require frequency-based correction factors to force their MT transfer functions computed from quiet-time data to match storm-time geoelectric field measurements.

In the case of dense MT surveys, like in the USA (Schultz et al., 2006–2018), the interpolation of impedances over the whole modelling domain becomes feasible and the estimation of the geoelectric field over larger areas is possible (Bonner & Schultz, 2017). This is desirable for the accurate modelling of GICs which requires the integration of electric fields along the affected ground infrastructure like power lines or pipelines which can extend over long distances crossing several regions of lateral conductivity variation. We will use the MT transfer functions to estimate geoelectric fields from historic large storm events (see Sect. 5).

4 Thin-sheet modeling of the geoelectric field

To model the regional geoelectric field, we wish to combine the response of the ground conductivity in a region with the spatial and temporal measurements of the rate of change of the horizontal components of the magnetic field. We use a thin-sheet model to do this which has the advantage that spatially variable magnetic fields can be used as an input. The modelling code is based upon the work of Vasseur & Weidelt (1977) which has been employed in previous studies noted in the Introduction. The code computes the surface electric field arising at a particular period (for example, 120 s or 2 min) from a 2-D conductivity model of the surface and a layered subsurface. Using a series of Green’s functions convolved with a two-dimensional thin-sheet representation of the conductance,
the effect that conductivity variations have on redistributing regional or “normal” currents induced elsewhere (for example, in the sea) can be computed. The surface layer can be regarded as an infinite thin-sheet of finite laterally-variable conductance, across which certain boundary conditions apply.

For the top layer, we use conductance values in a 10 km grid-cell model of the UK developed by Beamish & White (2012) and Beamish (2013). The lithology-based classification of bedrock is used to provide an association with the petrophysical rock parameters controlling bulk conductivity, assumed to represent the conductance to a depth of 3 km. The 10 km map is based on a reduced version of a 1:625 k scale (approximately 1 km) map, and is comprised of 86 lithological classifications. Offshore, seawater is assumed to have a conductivity of 3 S/m and the model accounts for changes in bathymetry. The model extends 1200 × 1680 km (121 × 169 cells) and, in order to reduce edge effects, an additional 5 cells of padding are added to each edge to make the final grid of 131 × 179 cells. The padding cells have values close to the average conductance of the entire model. Figure 6 (left panel) shows the 2D thin-sheet conductance map of the UK.

Below 3 km, a series of 1D models, each with 20 layers, are used to represent the underlying structure of the British Isles to a depth of approximately 1000 km. The shallow to mid-crustal tectonic setup of the UK can be described by six major geological terranes. We use the conductivities from the terrane model of Beamish et al. (2002), categorised as the more resistive Northern and Central Highlands and the less resistive Midland Valley and Southern Uplands of Scotland. South of the Iapetus Suture Zone covering much of England lies the Concealed Caledonides terrane with a conductive mid-crustal anomaly. The southern part of the UK is considered as part of the Variscan Zone. Adám et al. (2012) provide values for the 1D conductivity models of these terranes. Figure 6 (right panel) shows the resistivity of the models at a depth of 6.5 km. The influence of these underlying 1D models on the magnitude of the induced geoelectric field at the surface was examined in detail in Beggan (2015). We acknowledge that this lithospheric model is entirely synthetic and can in reality differ from the true threedimensional electrical conductivity distribution in the crust and upper mantle. In the absence of countrywide MT data, it is nevertheless a good first approximation using available data and geological information.

The code requires the average rate-of-change of the horizontal magnetic field for a fixed period as an input. Different strategies can be chosen to incorporate the magnetic field variation over the area of interest. In previous papers (e.g. Kelly et al., 2017), we have used the ΔB value of the external field recorded every minute at several observatories by assuming the amplitude of the horizontal field changes sinusoidally with a period of length T (in minutes), as an electrojet current system moves back and forwards in latitude, the input field strength (H₀) at any time (t) can be represented by $B_y = H_0 \sin(2\pi T/2)$. However, this does not impose any bandpass filtering on the input magnetic field and implies a fixed frequency on the output geoelectric field.

Instead, for this study, we adopted an alternative method suggested in Bailey et al. (2017, 2018) which uses the rate of change of the horizontal components of the field (dBₓ/dt and dBᵧ/dt). Their Austrian-based study used the difference in the magnetic values every 5 min (Δt = 300 s) and, in combination with a model of the country’s high voltage power network, successfully matched the GIC measurements at several sites in the country. We replicate this approach but using a difference of 2 min (Δt = 120 s) which matches the available magnetic time-series of minute-mean values. We also refer to Ivannikova et al. (2018) who showed that their thin-sheet geoelectric field model computed with a full 3D model to within 8% for periods longer than 50 s.

To implement this approach, maps of the magnetic field across the region are created for each minute of the day using spherical elementary current systems (SECS) to interpolate between measurement sites (Amm, 1997). The SECS method produces good estimates of the magnetic field across the modelling domain when there are typically greater than five observatories available in a closely spaced (<500 km) configuration. If there are more observatories available, the resulting interpolation improves (McLay & Beggan, 2010).

Fig. 6. Left panel: Thin-sheet conductance model of the UK and surrounding seas with a cell size of 10 km (units of log 10 (Siemens)). Right panel: Block model underlying the thin-sheet conductance model with electrical resistivities assigned according to geologic domains after Beamish & White (2012).
The difference of the magnetic field every 2 min is computed (giving 720 snapshots per day) and each snapshot of the magnetic field is passed into the thin-sheet code. The output consists of geoelectric maps for every 2nd min of the day. Note, we also tested $\Delta t$ of 5 and 10 min (300 and 600 s) and found similar patterns of variation, though with smaller amplitude ranges. In practice, we run the thin-sheet model for each of the 1D terrane models and combine the results by extracting the corresponding part of each terrane on land into the final model. This is, in effect, a blocky pseudo-3D approximation, similar to Myllys et al. (2014) or Viljanen & Pirjola (2017).

We can then test how well the thin-sheet geoelectric field values compare to the recorded measurements at the three observatories. However, there are a number of limitations, which include the extent of the thin-sheet model and the effect of regional or local geological features. In the first case, the thin-sheet model does not extend to the Lerwick Observatory, though it is quite close to the edge (around 20 km). To extract the geoelectric field at this site, we must extrapolate the thin-sheet model slightly, which introduces some additional uncertainty. At Eskdalemuir, it is well known that there is a shallow local crustal anomaly though this mostly affects the vertical magnetic component (Banks et al., 1996). Finally, Hartland is strongly influenced by a tidal geoelectric signal which is not captured by the thin-sheet model due to the band-pass filter applied to produce the $dB/dt$ values; however, we are interested primarily in the space weather effects which are demonstratively shorter-period (see Figs. 2–4).

5 Comparison between electric field models and measurements

We examine the geoelectric field modelled for three of the larger storms experienced in the UK between 2013 and 2018: 17–18 March 2015, 7–8 September 2017 and 26 August 2018. We compare the MT-derived and the thin-sheet model geoelectric field values against the measured data at the three UK observatories.

We isolate the external field part of the magnetic field by removing the average quiet-time mean value of magnetic component computed from measurements made a few hours prior to the storm’s initiation. For example, local night-time values between 02:00 and 03:00 LT a day or so prior to a storm are often the quietest. The external field will comprise ionospheric and magnetospheric sources as well as the magnetic effect of telluric currents which may be a relatively large contribution (Juuusola et al., 2020).

To compute the external magnetic field variation over the North Sea we used SECS with data from the three BGS observatories complemented with other observatory or variometer data from Ireland, the Faroe Islands, France, Germany, Belgium, Denmark and Norway in order to expand the region over which the external magnetic field can be computed. Figure 7 shows the spatial extent of the magnetic measurements available. Note not all stations are available for each storm (see Table 1). In general, we find using a larger number of magnetic observatories creates a better model of the magnetic field over the region, which in turn produces a better match between the measured and modelled geoelectric field. For the thin-sheet code this is related to a convolution and integration of the magnetic field with the conductivity model over the entire grid.

5.1 March 2015 storm

The first so-called “super” storm of solar cycle 24 was the St. Patrick’s Day storm, starting on the 17 March 2015 with the $\Delta$St index exceeding 200 nT (Wu et al., 2016). The storm followed a partial-halo Coronal Mass Ejection (CME), associated with an X-ray solar flare of moderate intensity (C9.1), that occurred on the surface of the Sun on 15 March 2015. The most rapid geomagnetic variations were associated with periods of strongly negative IMF $B_z$ of $-20$ nT. In the UK, the storm exhibited two main bursts of activity on the evening of the 17 March separated by around 6 h (see Fig. 2).

For the March 2015 storm, magnetic data from eight observatories were available, allowing interpolation of the magnetic field variation across the UK. The northernmost variometers are Dombås (DOB) and Karlsøy (KAR) in Norway, with Dourbes (DOU) in Belgium being the southernmost observatory. Wingst (WNG) is the east-most observatory and Valentia (VAL) is west-most. While not ideal for SECS interpolation, as there is no control in the northwestern region, the spatial distribution covers the majority of the thin-sheet modelling area.

The thin-sheet model was run using the north ($X$) component and east ($Y$) components of the external magnetic field variation for a response period of 120 s. In order to compare to the modelled field, the measured geoelectric field data were band-passed between 120 and 3600 s using a Butterworth 3-pole filter. As the geoelectric field data are recorded at 10 Hz, this removes much of the very short-period and some of the long period energy though as we noted in the previous section longer period variations do not have much influence on GIC.
Figure 8 shows the comparison of the geoelectric field measurements made at each observatory for the March 2015 storm. The measured data in blue, the MT-derived values are in green and the thin-sheet modelled values are in red. In Lerwick the geoelectric field variation reached over 1 V/km peak-to-peak around 18:00 UT in the east component, while it was around 50% smaller at Eskdalemuir with a peak-to-peak change of 500 mV/km. At the most southerly observatory, Hartland, the geoelectric field in this frequency band reaches around 50 mV/km peak-to-peak.

For the east component of the thin-sheet electric field at Lerwick the magnitude is not well captured, though the match is better in the north component. The MT values are closer, though do not match the peak values at all times. At Eskdalemuir, the thin-sheet comparison in phase and amplitude is much better in the north component compared to the east component, while in Hartland the magnitude is similar though the correlation is poorer (see Sect. 5.4 for further detail). As the east–west geoelectric field component of the thin-sheet model is poorest at the two northerly sites, it suggests a problem with modelling the variation of the magnetic field in these areas due to the limited spatial extent of ground stations used.

### 5.2 September 2017 storm

On 7 September 2017 one of the largest storms of the 24th solar cycle hit the Earth (Dimmock et al., 2019). A CME left the Sun at midday on 6 September and reached Earth’s magnetosphere around 36 h later. Starting about 23:30 UT on 7 September, the first and deepest part of the storm lasted for around 3 h, reaching a Dst of −124 nT. At 13:00 UT on 8 September a second substorm was triggered, though not as large as the first part of the storm (Fig. 3).

To get a regional picture of the storm, data were collected from a network of Raspberry Pi magnetometers (denoted BGS3/7/9/10) (Beggan & Marple, 2018), as well as a number of other variometers and observatories around the UK, Ireland, Belgium, Germany and Norway including the observatories (from INTERMAGNET), the Lancaster University Aurora-Watch network of variometers (Case et al., 2017), a network in Ireland run by Trinity College Dublin (MagIE) (Blake et al., 2016) and data from the Tromsø Geophysical Observatory (TGO) network. The SOL and KAR sites host calibrated variometers which provide the variation of the field in addition the absolute values of the geomagnetic field vector, though the data are not as well controlled as at full observatories (where weekly baseline measurements are conducted). We also received data from the DTU-operated Faroe Islands Hov variometer, which helped to constrain the field variations in the northwestern area of the model. In total, magnetic data from twenty sites were collected, giving an excellent representation of the magnetic field variation across Britain and Ireland. As before, data were processed to remove the quiet time mean value of the horizontal components at each site, using the value for 02:00–03:00 local time from 7 September. Where the orientation of the sensor is unknown (as with the Raspberry Pi magnetometers) we rotated the quiet time horizontal components to match the estimated values of X and Y from a global magnetic field model, the 12th generation of the International Geomagnetic Reference Field (Thébault et al., 2015). The thin-sheet model was run for the storm using two days’ worth of magnetic values for both the X and the Y magnetic field components.

Figure 9 shows the resulting band-pass filtered thin-sheet model output compared to the band-passed measurements of the geoelectric field from each observatory. The intensity of the September storm is comparable to, if not larger than, the March 2015 storm in terms of the peak-to-peak variations at each observatory. The plots show the two large substorms around midnight of the 7th September and 12:00–18:00 on the 8th. The electric field variation is over 1 V/km in Lerwick, 500 mV/km in Eskdalemuir and 80 mV/km in Hartland. Note that the large values in Hartland around 21:00 on the 8th are an artefact.

For this storm, the thin-sheet model has performed better in capturing the magnitude and phase of the geoelectric field at all three sites. The MT values provide a good estimate of the geoelectric field too, matching best at Eskdalemuir and Hartland. We provide a more comprehensive quantitative evaluation of the data fit see Section 5.4.

### 5.3 August 2018 storm

Although the August 2018 storm was a relatively small event in the solar cycle, it was the largest storm of the year with a peak Kp of 7+. The total interplanetary magnetic field reached a strength of 21 nT with a prolonged period of southward $B_z$ and the Dst index had a peak of −174 nT. The storm was likely caused by a CME though no classic shock signature was observed. The storm coincided with the deployment of differential magnetometer method (DMM) system which allowed a detailed analysis of GICs in the 400 kV high voltage power grid in East Scotland (Hubert et al., 2020).

For the magnetic field interpolation, fewer variometers were available for this storm (only 10 stations, e.g. due to maintenance issues), so the SECS model of the field is not as accurate as for the September 2017 storm. Magnetic data are available from Hov in the Faroe Islands in the north to Dourbes in Belgium to the south and we include some of the AuroraWatch

| Storm   | Stations                              |
|---------|---------------------------------------|
| Mar 2015 | DOB, DOU, ESK, HAD, KAR, LER, VAL, WNG |
| Sep 2017 | ARM, BIR, BGS3, BGS7, BGS9, CRK, DOB, DOU, ESK HAD, HOV, KAR, LAN, LER, SID, SOL, SUM, VAL, WNG |
| Aug 2018 | BGS10, CRK, DOU, ESK, HAD, HOV, LER, SOL, VAL, WNG |
| Mar 1989 | CRK, ESK, HAD, LER, VAL, WNG |
| Oct 2003 | CRK, DOB, DOU, ESK, HAD, FAR, KAR, LER, VAL, WNG |
and BGS school magnetometer data. In addition, as noted in Section 2, the geoelectric field probes at LER, ESK and HAD only have data from one channel available at each site, due to a mixture of equipment failure and probe degradation.

Figure 10 shows the measured, MT-derived and thin-sheet modelled geoelectric field values. The overall magnitude of the field is much smaller than during the other two storms examined. Lerwick has a peak-to-peak variation of around 250 mV/km in the north component, while Eskdalemuir reaches around 100 mV/km in the east component. The geoelectric field in Hartland is very small, barely exceeding 20 mV/km peak-to-peak. Similar to March 2015, the north component of Lerwick is poorly captured by the thin-sheet model in the main phase. The E–W geoelectric field component at Eskdalemuir is better

Fig. 8. Comparison of the thin-sheet (TS), magnetotelluric (MT impedance) and measured geoelectric field at (a, b) Lerwick, (c, d) Eskdalemuir and (e, f) Hartland observatories for 17 March 2015.
modelled, though not as well as the September 2017 storm, while Hartland has very small geoelectric field values and so the comparison is difficult to judge.

5.4 Metrics to assess data fit between measured and modelled electric field data

When comparing relatively “noisy” data sets such as the geoelectric field values, it is difficult to provide an over-arching metric that best describes the match between the model and measurements as minor fluctuations in the local geoelectric field cannot be captured by the regional model. This means that direct correlations between the time-series can be low despite appearing close.

To account for this we use a selection of metrics to assess quantitatively how well the models match the measurements. As well as the standard correlation between the time-series, following Torta et al. (2014), we compute the $P$-metric for each storm using:

$$P = 1 - \frac{\text{RMSD}_{\text{on}}}{\sigma_{o}}$$

Fig. 9. Comparison of the thin-sheet (TS), magnetotelluric (MT impedance) and measured geoelectric field at (a, b) Lerwick, (c, d) Eskdalemuir and (e, f) Hartland observatories for 7–8 September 2017.
where \( \sigma \) is the standard deviation of the set of observations and RMSD_{om} is the root mean square deviation of the residuals (i.e. differences between model predictions and observations),

\[
\text{RMSD}_{om} = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (o_i - m_i)^2}.
\]

The values \( o_i \) and \( m_i \) are the \( i \)th point (of \( N \) samples) of the observation and model. The maximum value of \( P \) cannot exceed 1 where the model exactly fits the observations. However, if \( P \) is zero or less there is little direct predictive power, though a negative value of \( P \) does not necessarily imply an anti-correlation. Torta et al. (2014) examined time-series of GIC measurements versus GIC models in the Spanish power transmission grid and found that rarely did \( P \) exceed 0.4, even with visually close match between their time-series.

Table 2 gives a series of metrics for the correlation of the measured data and thin-sheet time-series shown in Figures 8–10. For the March 2015 storm, the correlation is surprisingly high for the north–south component of Lerwick and Eskdalemuir at 0.68 and 0.58, but is around zero for Hartland. The \( P \) values for Lerwick and Eskdalemuir are very small though (0.09 and 0.17).

The September 2017 storm shows again that the correlation can be high though the \( P \) metric is negative. For Eskdalemuir in the N–S component, there is a good match between the time-series but it has a \( P \) value of \(-0.25\) with a correlation of 0.59. Finally, the thin-sheet electric field estimates for the August 2018 storm are moderately correlated for Lerwick (0.54) and Eskdalemuir (0.47) but low for Hartland (0.25).

### Table 2. Metric comparisons for three storms with thin-sheet-derived geoelectric field values.

| Storm  | Metric   | LER (N–S) | LER (E–W) | ESK (N–S) | ESK (E–W) | HAD (N–S) | HAD (E–W) |
|--------|----------|-----------|-----------|-----------|-----------|-----------|-----------|
| Mar-15 | RMSD_{om} | 114.4     | 41.8      | 19.3      | 39.5      | 6.4       | 6.5       |
|        | \( P \)     | 0.09      | 0.01      | 0.17      | 0.06      | \(-0.29\) | \(-0.24\) |
|        | Correlation | 0.68      | 0.24      | 0.58      | 0.33      | \(0.01\)  | \(-0.07\) |
| Sep-17 | RMSD_{om} | 45.6      | 96.0      | 18.9      | 19.8      | 5.0       | 6.0       |
|        | \( P \)     | 0.18      | \(-0.01\) | \(-0.25\) | 0.24      | \(-0.13\) | \(-0.02\) |
|        | Correlation | 0.58      | 0.32      | 0.59      | 0.66      | 0.44      | 0.46      |
| Aug-18 | RMSD_{om} | 18.0      | \(-\)      | \(-\)      | 6.4       | 2.2       | \(-\)      |
|        | \( P \)     | 0.15      | \(-\)      | \(-\)      | \(0.08\)  | \(-0.05\) | \(-\)      |
|        | Correlation | 0.54      | \(-\)      | \(-\)      | 0.47      | 0.25      | \(-\)      |

Fig. 10. Comparison of the thin-sheet (TS), magnetotelluric (MT impedance) and measured geoelectric field at (a) Lerwick, (b) Eskdalemuir and (c) Hartland observatories for 26 August 2018. Note only one channel was available at each site.
For the MT-derived geoelectric field time-series, the correlations with the measured values are given in Table 3. Again, the correlations with each observatory are very high (generally 0.75–0.95), as expected, as the impedance functions are derived from the measurements at each site. However, the $P$ values are quite mixed from −0.24 at Lerwick for the March 2015 storm to 0.56 for Eskdalemuir during the same storm. Hence, even if the correlation is high, the time-series can also have a low $P$ value when there is a large difference in the magnitude.

The differences between the measurements and models can be large and occasionally similar in magnitude. The metric tables illustrate this point – that the correlation between the models can be good but the $P$ metric is often not high and occasionally close to zero, a direct comparison of the models and measurements is shown in Figure 11. The differences between the measured values of the geoelectric field and those modelled by thin-sheet and MT method for the 7/8th September 2017 at Eskdalemuir are plotted. The north–south direction of the thin-sheet model has a negative $P$ value (−0.25) even though the correlation is quite high (0.59) (see Fig. 9). In contrast, the east–west component has $P$ value of 0.24 with a correlation of 0.66. This is an example where the phase of the

### Table 3. Metric comparisons for three storms with the impedance-derived geoelectric field values.

| Storm | Metric  | LER (N–S) | LER (E–W) | ESK (N–S) | ESK (E–W) | HAD (N–S) | HAD (E–W) |
|-------|---------|-----------|-----------|-----------|-----------|-----------|-----------|
| Mar-15| RMSD$_{om}$ | 27.58 | 50.67 | 11.21 | 8.2 | 1.75 | 2.0 |
|       | $P$     | −0.24 | 0.36 | 0.56 | 0.42 | 0.50 | 0.39 |
|       | Correlation | 0.79 | 0.89 | 0.95 | 0.90 | 0.94 | 0.92 |
| Sep-17| RMSD$_{om}$ | 25.5 | 33.6 | 8.3 | 4.7 | 2.3 | 1.89 |
|       | $P$     | 0.15 | 0.6 | 0.48 | 0.53 | 0.16 | 0.38 |
|       | Correlation | 0.91 | 0.92 | 0.97 | 0.95 | 0.88 | 0.94 |
| Aug-18| RMSD$_{om}$ | 16.1 | – | – | 5.5 | 2.4 | – |
|       | $P$     | −0.03 | – | – | 0.24 | −0.28 | – |
|       | Correlation | 0.76 | – | – | 0.76 | 0.52 | – |

**Fig. 11.** The measured geoelectric field (blue, offset from zero) and differences between it and the thin-sheet (red) and magnetotelluric (green) models at ESK for the 7–8 September 2017.
The geoelectric field variation is well captured by both models, but the magnitude is not.

### 6 Historic storms

Using the MT impedance functions for each site, the one-minute-mean magnetic field measurements from the 13–14 March 1989 to 29–31 October 2003 were used to estimate the geoelectric field (Campanya et al., 2019; Hübert et al., 2020). The main limitation of this approach is the plane-wave assumption of the magnetic field for the MT response functions, which is generally applicable only for geomagnetically quiet times at mid to low latitudes.

Figure 12 shows the geoelectric field values for both storms computed from the MT impedance and the thin-sheet modelling code. For the thin-sheet model, fewer observatory data were available compared to the analyses in Section 4 (see Table 1) so the magnetic field is not as well captured across the region. For the MT-derived values, the March 1989 storm has electric field amplitudes of up to 1 V/km at Lerwick in the north–south component, around midnight on 13 March, and 2.3 V/km in the east–west component. The geoelectric field at Hartland does not exceed 0.16 V/km. The thin-sheet model shows similar magnitude peaks though generally around 30% lower (e.g., 0.7 V/km compared to 1 V/km in Lerwick north component).

For the October 2003 storm, the estimated geoelectric fields overall are slightly smaller. Eskdalemuir experienced larger values in the north–south component compared to Lerwick late on the 30th October with one large period of almost 3 V/km. The larger magnetic (and hence geoelectric) fields experienced at Eskdalemuir in the north–south component may be related to rapid expansion of the auroral oval during storm times (Freeman et al., 2019). The geoelectric field values for Hartland are generally small for both storms and indeed not much larger than those measured during the September 2017 storm for example.

### 7 Discussion

Measurements of the magnetic and geoelectric field at the three UK observatories illustrate that the Earth acts as a high-pass filter during geomagnetic storms, removing much of the long magnetic field period variation beyond 1 h. Between 2012 and 2020, the maximum absolute value of the
magnetic observatory and variometer data to create a good representation of the high voltage network model at Torness in Hübert et al. (2019) and Lucas et al. (2020).

8 Conclusions

The geoelectric field is a key driver of geomagnetically induced currents in grounded infrastructure. Successfully modelling this field is essential for providing real-time estimates of hazard to the high voltage power network. Due to the diverse geological and topographical structure of the UK, the geoelectric field varies in a complex manner, both spatially and temporally.

We describe the three main strands of research to understand and model the geoelectric field in the UK during severe space weather events. Firstly, continuous measurements of the geoelectric field at a cadence of 10 Hz have been on-going at the three UK observatories since 2012. Although several major storms have been observed between 2012 and 2020, none have been large enough to cause known issues with technical infrastructure. The largest absolute magnitude of the geoelectric field measured was around 1 V/km at Lerwick in March 2015.

Modelling using the thin-sheet methodology allows us to compute near-real-time estimates of the field though at the cost of reduced accuracy. From comparison with geoelectric measurements at three observatories, we conclude the thin-sheet model provides some predictive power, though this is typically an underestimate of the true value of the geoelectric field.

Future work will involve updating the geoelectric probes at each observatory as the original hardware reaches the end-of-life, installing new variometers in the UK and to continue to collect magnetotelluric data from sites around Britain to aid the modelling of geoelectric fields for real-time and forecasting applications.

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