Describing SGRs/AXPs as fast and magnetized white dwarfs

M. Malheiro* and J. G. Coelho
Instituto Tecnológico de Aeronáutica
Departamento de Ciência e Tecnologia Aeroespacial
12228-900 Vila das Acácias
São José dos Campos, SP
Brazil
*Email: malheiro@ita.br

1 Introduction

Over the last decade, observational evidence has mounted that SGRs/AXPs belong to a particular class of pulsars. Furthermore, fast and very magnetic white dwarfs have been observed, and recently two SGRs with low magnetic fields \(B \sim (10^{12} - 10^{13})\) G, namely SGR 0418+5729 and Swift J1822.3-1606 were discovered with a period of \(P \sim 9.08\) s and \(P \sim 8.44\) s, respectively [1, 2]. These new discoveries opens the question of the nature of SGRs/AXPs, emerging alternative scenarios, in particular the white dwarf (WD) pulsar model [3, 4, 5, 6]. These astronomical observations have based an alternative description of the SGRs/AXPs expressed on rotating highly magnetized and very massive WDs (see Malheiro et al. 2012 for more details of this model [3]).

As pointed out in [5], in this new description, several observational properties are easy understood and well explained as a consequence of the large radius of a massive white dwarf that manifests a new scale of mass density, moment of inertia, rotational energy, and magnetic dipole moment in comparison with the case of neutron stars.

In this contribution, we will show that these recent discoveries of SGRs with low magnetic field share some properties with the recent detected fast WD pulsar AE Aquarii, and also with RXJ 0648.0-4418, and EUVE J0317-855, supporting the understanding of at least these SGRs with low-B as belonging to a class of very fast and magnetic massive WDs. Furthermore, these recent astronomical observations suggest that we should revisit the real nature of AXP/SGRs: are they really magnetars or very fast and massive white dwarfs? In the next section, we present an overview about this model, and in Section 3 we discuss the recent observations of SGRs with low magnetic field and the recent observations of fast and magnetized white dwarfs, and in particular the AE Aquarii as the first white dwarf of a new family of spin-powered white dwarf pulsars.
A new interpretation - white dwarf pulsar model

As already discussed in Coelho & Malheiro 2012 [4, 5], the magnetic field at the magnetic pole $B_p$ of the star is related to the dipole magnetic moment by,

$$| \vec{m} | = \frac{B_p R^3}{2},$$  \hspace{1cm} (1)

where $R$ is the star radius. If the star magnetic dipole moment is misaligned with the spin axis by an angle $\alpha$, electromagnetic energy is emitted at a rate (see e.g., Shapiro and Teukolsky [7] and references therein),

$$\dot{E}_{\text{dip}} = -\frac{2}{3c^3} | \vec{m} |^2 = -\frac{2}{3c^3} | \vec{m} |^2 \omega^4 \sin^2 \alpha,$$  \hspace{1cm} (2)

where $\omega$ is the star angular rotational frequency. Thus, it is the magnetic dipole moment of the star, the physical quantity that dictates the scale of the electromagnetic radiated power emitted, besides with the angular rotational frequency. The fundamental physical idea of the rotation-powered pulsar is that the X-ray luminosity - produced by the dipole field - can be expressed as originated from the loss of rotational energy of the pulsar,

$$\dot{E}_{\text{rot}} = -4\pi^2 I \frac{\dot{P}}{P^3},$$  \hspace{1cm} (3)

associated to its spin-down rate $\dot{P}$, where $P$ is the rotational period and $I$ is the momentum of inertia.

Thus, equaling Eqs. (2) and (3) we deduce the expression of pulsar magnetic dipole moment,

$$m = \left( \frac{3c^3 I}{8\pi^2} P \dot{P} \right)^{1/2},$$  \hspace{1cm} (4)

From Eq. (1) we obtain the magnetic field at the equator $B_e$ as [8]

$$B_e = B_p/2 = \left( \frac{3c^3 I}{8\pi^2 R^6} \dot{P} \right)^{1/2},$$  \hspace{1cm} (5)

where $P$ and $\dot{P}$ are observed properties and the moment of inertia $I$ and the radius $R$ of the object model dependent quantities. The description commonly addressed as magnetar model [9, 10] is based on a canonical neutron star of $M = 1.4M_\odot$ and $R = 10$ km and then $I \sim 10^{45}$g cm$^2$ as the source of SGRs and AXPs. From Eqs. (4) and (5), and using the parameters above, we obtain the magnetic dipole moment and the magnetic field of the neutron star, respectively,

$$m_{\text{NS}} = 3.2 \times 10^{37} (P \dot{P})^{1/2} \text{emu},$$  \hspace{1cm} (6)
\[ B_{\text{NS}} = 3.2 \times 10^{19} (P \dot{P})^{1/2} \text{G}. \] (7)

For the case of the white dwarf model we use a radius \( R = 3000 \text{ km} \) for all SGRs and AXPs and a mass \( M = 1.4 M_\odot \), as recent studies of fast and very massive white dwarfs obtained (see K. Boshkayev et al. 2012 [11]). Thus, these values of mass and radius generating the momentum of inertia \( I \sim 1.26 \times 10^{50} \text{g cm}^2 \), will be adopt hereafter in this work as the fiducial white dwarf model parameters. Using that parameters we obtain the magnetic dipole moment and the magnetic field of the white dwarf pulsar, respectively,

\[ m_{\text{WD}} = 1.14 \times 10^{40} (P \dot{P})^{1/2} \text{emu}, \] (8)

and

\[ B_{\text{WD}} = 4.21 \times 10^{14} (P \dot{P})^{1/2} \text{G}. \] (9)

These results clearly shows that the scale of the dipole magnetic moment in WD is \( \sim 10^3 \) times larger than for neutron stars, exactly the factor seen in the X-ray luminosity of SGRs/AXPs when compared with \( L_X \) of slow pulsars (\( P \sim 1 \) to 10 s) as X-ray Dim isolated neutron stars (XDINs) and high-B radio pulsars (see Coelho & Malheiro 2012 [5]). Furthermore, the surface magnetic field of WDs is \( \sim 10^5 \) smaller than the ones of neutron stars, eliminating all the overcritical \( B \) fields deduced in the magnetar model. Then, the basic idea is that, being a WD \( \sim 10^3 \) times bigger than a NS, at comparable mass, its moment of inertia is \( \sim 10^5 \) times larger. This implies that the rotational energy lost can be large enough to explain the observed X-ray luminosity in SGRs/AXPs (\( \sim 10^{32} - 10^{36} \text{ erg/s} \)) even for quite low values of the period derivative \( \dot{P} \).

3 Observations of magnetized white dwarfs and SGRs with low B

Magnetized white dwarfs (MWDs) constitute at least 10% of the white dwarfs if observational biases are considered [12]. The current known population of MWDs has been increased considerably by the Sloan Digital Sky Survey (SDSS) to about 220 objects (see Külebi et al. 2013 [13] for more details). SDSS also dramatically increased the total known white dwarf population (see e.g. Kleinman et al. 2013, for Data Release 7 [14]) and recent studies indicate that the number of MWDs in the SDSS could be as large as 521 [15, 13]. Furthermore, some sources have even been tentatively proposed as candidates for white dwarf pulsars. A specific example is AE Aquarii, the first white dwarf pulsar, very fast with a short period \( P = 33.08 \text{ s} \) [16 [17]. The rapid braking of the white dwarf and the nature of pulse hard X-ray emission detected with japanese SUZAKU space telescope under these conditions can
be explained in terms of spin-powered pulsar mechanism. Although AE Aquarii is in a binary system with orbital period $\sim 9.88$ hr, and not an isolated pulsar: very likely the power due to accretion of matter is inhibited by the fast rotation of the white dwarf [18].

Recently, Mereghetti et al. 2009 [19] showed that the X-ray pulsator RX J0648.0-4418 is a white dwarf with mass $M = 1.28M_\odot$ and radius $R = 3000$ km, and spin period $P = 13.2$ s. EUVE J0317-855, is another WD pulsar candidate discovered recently [20]. However, relevant pulse emission has not been observed yet, which may suggest that the electron-positron creation and acceleration does not occur (see Kashiyama et al. [21]). Barstow et al. 1995 [22] obtained a period of $P \sim 725$ s, which is also a fast and very magnetic WD with a dipole magnetic field is $B \sim 4.5 \times 10^8$ G (obtained by optical photometric and polarimetric), and a mass $(1.31 - 1.37)M_\odot$ which is relatively large compared with the typical WD mass $\sim 0.6M_\odot$. In this work, we describe AE Aquarii and RX J0648.0-4418 as a rotation powered white dwarf, and obtain the magnetic field, using the white dwarf parameters presented in the last section.

In Fig. 1, we present the magnetic field as a function of the period of these two SGRs with low B described in the white dwarf model with the three fast white dwarfs presented above. Here we see that the magnetic field $B$ of the SGRs and AXPs as NSs or WDs are quite different ($\sim 10^5$ order of difference) as explained in the last section, and already pointed out in Refs. [3, 4, 5]. The magnetic field $B$ of the two recent SGRs described as white dwarf pulsars are comparable with the ones observed for the fast white dwarfs also plotted. The magnetic WDs shown in Fig. 1 are the complete sample obtained by SDSS project, for which the period $P$ and magnetic field $B$ are known. The magnetic fast white dwarfs are separated in two classes: isolated and polars, very magnetic with $B \sim (10^7 - 10^8)$ G, and the intermediate polars with weaker field $B \sim 10^5$ G.

In Table 1 we compare and contrast the parameters of these three fast white dwarfs with the two SGRs with low B described in the white dwarf model presented before. As already shown in Ref. [4, 5], important features of the two SGRs with low magnetic field are very similar to the ones of fast and magnetic white dwarfs recently detected. They are old, characteristic ages of Myr, low quiescent X-ray luminosity $L_X \sim (10^{30} - 10^{32})$, magnetic field of $B_{WD} \sim (10^7 - 10^8)$ G and magnetic dipole moments of $m_{WD} \sim (10^{33} - 10^{34})$ emu. These results give evidence for the interpretation of SGRs/AXPs as being rotating white dwarf pulsars, at least the two SGRs with low-B.
Figure 1: The figure shows the magnetic field strength of neutron stars and magnetic white dwarfs as a function of the rotational period.

|            | SGR 0418 | Swift J1822 | AE Aquarii | RXJ 0648 | EUVE J0317 |
|------------|----------|-------------|------------|----------|------------|
| $P (s)$    | 9.08     | 8.44        | 33.08      | 13.2     | 725        |
| $\dot{P} \times 10^{-14}$ | 0.4      | 8.3         | 5.64       | < 90     | -          |
| Age (Myr)  | 24       | 1.6         | 9.3        | 0.23     | -          |
| $L_X$ (erg/s) | $\sim 1.0 \times 10^{30}$ | $\sim 4.2 \times 10^{32}$ | $\sim 10^{31}$ | $\sim 10^{32}$ | -         |
| $B_{WD}$ (G) | $\sim 8.02 \times 10^{7}$ | $\sim 3.52 \times 10^{8}$ | $\sim 5 \times 10^{7}$ | $< 1.45 \times 10^{9}$ | $\sim 4.5 \times 10^{8}$ |
| $B_{NS}$ (G) | $\sim 6.10 \times 10^{12}$ | $\sim 2.70 \times 10^{13}$ | -          | -        | -          |
| $m_{WD}$ (emu) | $\sim 2.17 \times 10^{33}$ | $\sim 0.95 \times 10^{34}$ | $\sim 1.35 \times 10^{33}$ | $3.48 \times 10^{34}$ | $1.22 \times 10^{34}$ |
| $m_{NS}$ (emu) | $\sim 6.10 \times 10^{30}$ | $\sim 2.70 \times 10^{31}$ | -          | -        | -          |

Table 1: Comparison of the observational properties of five sources: SGR 0418+5729 and Swift J1822.3-1606 (see N. Rea et al. 2010, 2012) and three observed white dwarf pulsar candidates. For the SGR 0418+5729 and Swift J1822.3-1606 the parameters $P$, $\dot{P}$ and $L_X$ have been taken from the McGill online catalog at \url{www.physics.mcgill.ca/pulsar/magnetar/main.html}. The characteristic age is given by $Age = P/2\dot{P}$ and the magnetic moment $m$ and the surface magnetic field $B$ are given by Eqs. (4) and (5), respectively.

JGC and MM acknowledges the Brazilian agency FAPESP (thematic project 2007/03633-3), CNPq and CAPES. We are grateful to Y. Terada by the data points of the figure in this paper, and also by the valuable discussions.
References

[1] N. Rea, P. Esposito and R. Turolla et al., Science, 330, 944 (2010).
[2] N. Rea, G. L. Israel, P. Esposito et al., ApJ, 754, 27 (2012).
[3] M. Malheiro, J. A. Rueda and R. Ruffini, PASJ 64, 56 (2012).
[4] J. G. Coelho and M. Malheiro, IJMP. Conf. Ser., 18, 96 (2012).
[5] J. G. Coelho and M. Malheiro, ArXiv:1211.6078 (2012).
[6] J. G. Coelho and M. Malheiro, AIP Conf. Ser., 1520, 258 (2013).
[7] S. L. Shapiro and S. A. Teukolsky, Black Holes, White Dwarfs and Neutron Stars: The Physics of Compact Objects, 1 edn. (Wiley-VCH, 1983).
[8] A. Ferrari and R. Ruffini, ApJ, 158, L71+ (1969).
[9] R. C. Duncan and C. Thompson, ApJL, 392, L9 (1992).
[10] C. Thompson and R. C. Duncan, MNRAS, 275, 255 (1995).
[11] K. Boshkayev, J. A. Rueda, R. Ruffini and I. Siutsou, ApJ, 762, 117, (2012).
[12] A. Kawka, S. Vennes, G. D. Schmidt and D. T. Wickramasinghe, ApJ, 654, 499 (2007).
[13] B. Külebi, J. Kalirai, S. Jordan, and F. Euchner, arXiv: 1304.7171v1, (2013).
[14] S. J. Kleinman, S. O. Kepler, D. Koester et al., ApJS, 204, 5 (2013)
[15] S. O. Kepler, I. Pelisoli, S. Jordan et al., MNRAS, 429, 2934 (2013)
[16] Y. Terada, T. Hayashi, M. Ishida et al., PASJ, 60, 387 (2008c).
[17] J. R. P. Angel, E. F. Borra and J. D. Landstreet, ApJS, 45, 457 (1981).
[18] N. R. Ikhsanov and N. G. Beskrovnaya, Astronomy Reports, 56, 595 (2012).
[19] S. Mereghetti et al., Science, 325, 1222 (2009).
[20] B. Külebi et al., A&A, 524, A36 (2010b).
[21] K. Kashiyama, K. Ioka and N. Kawanaka, PRD, 83, 023002 (2011).
[22] M. A. Barstow et al., MNRAS, 277, 971 (1995).