Modelling co-translational dimerization for programmable nonlinearity in synthetic biology

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Nonlinearity plays a fundamental role in the performance of both natural and synthetic biological networks. Key functional motifs in living microbial systems, such as the emergence of bistability or oscillations, rely on nonlinear molecular dynamics. Despite its core importance, the rational design of nonlinearity remains an unmet challenge. This is largely due to a lack of mathematical modelling that accounts for the mechanistic basis of nonlinearity. We introduce a model for gene regulatory circuits that explicitly simulates protein dimerization—a well-known source of nonlinear dynamics. Specifically, our approach focuses on modelling co-translational dimerization: the formation of protein dimers during—and not after—translation. This is in contrast to the prevailing assumption that dimer generation is only viable between freely diffusing monomers (i.e. post-translational dimerization). We provide a method for fine-tuning nonlinearity on demand by balancing the impact of co- versus post-translational dimerization. Furthermore, we suggest design rules, such as protein length or physical separation between genes, that may be used to adjust dimerization dynamics in vivo. The design, build and test of genetic circuits with on-demand nonlinear dynamics will greatly improve the programmability of synthetic biological systems.

1. Introduction

Synthetic biology [1–3] is a growing field of research that uses engineering principles to design and implement human-defined computations in living cells. The development of complex mathematical modelling techniques [4,5], along with the advances in DNA synthesis and assembly [6], allows for the making of new-to-Nature networks of regulatory proteins—the so-called genetic circuits—with increasing information processing abilities. Relatively simple models of computation, like combinatorial [7] and sequential logic [8], have been successfully implemented in organisms such as bacteria [9], yeasts [10] or even mammalian cells [11]. Examples of these genetic circuits include logic gates [12,13], multiplexers [14], half-adders [15], counters [16] and memories [17]—and even more complex processes such as analogue [18,19] and distributed computations [20–22]. As well as generating fundamental insights into the workings of living systems, this (and many more) engineered system finds a broad range of applications in biotechnology and bioengineering [23,24]. Nevertheless, it could be argued that the field is in its infancy, since the vast differences between traditional silicon-based hardware and biological substrates suggest that there are powerful models of computation yet to be developed [25]. That is, the way synthetic constructs process information cannot get even close to that of natural biological systems.
Mathematical modelling, an essential component of synthetic biology, aids the design of increasingly complex genetic circuits by providing predictions of their dynamical performance [26,27]. By modelling the dynamics of gene expression (i.e. mechanistic steps going from genes to proteins), designs can be improved with information such as which DNA components are predicted [28] to perform better for a specific target function. That is, models answer questions that are difficult, if not at all impossible, to answer otherwise. However, the predictive power of models depends on the detail of the description of the physical processes they represent. There is one such process that, despite being of fundamental importance for genetic circuits and biological computation, has received relatively little attention to this end: the mechanistic understanding of nonlinear dynamics [29–32]; specifically, because of its relevance for genetic circuits, the nonlinearity that emerges from the dimerization of regulatory proteins [33]. Although dimerization is a well-known source of nonlinear dynamics, current mathematical models fail to provide a mechanistic description of it. The goal of this study is to overcome such limitations. Upon gene expression, most resulting proteins are monomers that need to interact to form dimers (or higher-order oligomers); it is only the protein in its final from that is active. Furthermore, dimerization is intertwined with other sources of nonlinearity [34], such as regulator–promoter interplay [35] (known as bursting). In the early days of synthetic biology, two landmark papers demonstrated that such nonlinear dynamics are at the core of relatively simple circuits. The first one implemented a ‘toggle switch’ [36]: a genetic circuit able to switch between two states according to external signals. The second one implemented what was called the ‘repressilator’ [37]: an oscillator based on a circuit of gene transcription repressors. Mathematical models of these two circuits show bistability and reliable oscillations (respectively) only if they account for nonlinear dynamics.

A non-trivial issue is that protein monomers have to meet in order for dimerization to happen. But, where do they meet? Nearly, 30 years ago, a paper titled [...] it takes two to tango but who decides [...] on the venue? [38] fired this question explicitly; soon after, another paper found experimental evidence for what they called co-translational dimerization [39]. The latter work established a difference between co-translational, which takes place during translation (from RNA into proteins), and post-translational dimerization pathways. However, current mathematical modelling accounts for the dimerization of proteins using abstract parameters without physical description. These parameters do not have a direct physical translation, which is abstracted away. That is, the values of these parameters do not inform us about specific mechanistic details that could be engineered in vivo. While Michaelis–Menten equations, for instance, use integer values for a physical parameter, Hill equations allow for unphysical non-integer values. Although somewhat effective, these modelling approaches abstract away dimerization into a black box, thus hiding it from the design process. The lack of description of the molecular details of non-linearity limits the rational design of such behaviour. In contrast to prevailing approaches, our model aims at breaking that abstraction by providing parameters with direct physical interpretation. Therefore, the values of the parameters presented below correspond to the rules and principles that can be applied at the design stage in order to engineer a DNA device with an on-demand nonlinear behaviour.

2. Results and discussion

2.1. A model for co-translational dimerization

Transcription (of a gene into RNA) and translation (of RNA into proteins) rarely generate fully functional transcriptional regulators. Rather, the resulting proteins—or ‘monomers’—need to interact with others in order to form ‘dimers’ (figure 1a); for example, the repressor protein TetR, which is extensively used in synthetic biology, is a dimer. This suggests that any mathematical model that aims at simulating the dynamics of such a molecule (or that of a genetic circuit regulated by it) must account for the dimerization of the partially formed regulators generated after translation in order to result in robust predictions.

Although typical modelling frameworks, such as Michaelis-Menten and Hill equations, already account for dimerization, matching this to its specific molecular mechanisms and features (in contrast to using abstract cooperativity values) is still an overarching challenge. Our model adds a detailed mechanism of translation, in which ribosomes bind RNA molecules in an asynchronous fashion; as a result, some ribosomes start translating very close to each other [40]. In this scenario, two partially formed monomers come into contact and dimerization starts, which has been termed co-translational dimerization (figure 1b) [39]. When ribosomes are at a long-enough distance apart, dimerization will take place in the cytoplasm (i.e. post-translational dimerization), where both monomers must meet before building a dimer. The model presented here accounts for these...
dynamics, which, in turn, shape the nonlinearity features (in final dimer formation) of the genetic circuit at stake.

In order to describe co-translational dimerization rates, the model first assumes that the arrival of a ribosome at the RNA is captured by a Poisson point process since discrete events occur independently at a given rate. The distribution of time between binding events (P(Δt)) is then given by the following equation:

\[ P(\Delta t) = \lambda \cdot e^{-\lambda \Delta t}, \quad (2.1) \]

where \( \lambda \) is the average binding rate of a ribosome to the RNA (i.e., when translation initiates), and \( \Delta t \) represents the time between such binding events. This time distribution, along with the experimentally obtained translation rate of \( \alpha \) 10 AA s\(^{-1}\) [41,42] (AA = amino acids), was used to calculate the distance between two consecutive ribosomes (\( \Delta x \)) and the length difference of the partially translated monomers being generated by them (\( \Delta \lambda \)).

\[ \Psi(\Delta t, \lambda) = \left\{ \begin{array}{ll} \left( \frac{\Delta x - \sqrt{\Delta x^2 + \Delta r^2}}{16\Delta x^2} \right)^2 & \text{if } \Delta r + 2r > \Delta x \\ \frac{\Delta r + 2r \leq \Delta x}{16\Delta x^2} & \end{array} \right. \quad (2.2) \]

where the output is a relative value going from 0 (no overlap at all) to 1 (complete overlap of partially formed monomers), \( \Delta x \) is the distance between two ribosomes and \( r \) is the current length of the least transcribed monomer (see Methods for model derivation). The creation of dimers at each specific time difference and at a specific protein length is assumed to obey Michaelis–Menten dynamics. Therefore, the calculation of the fraction of dimerization during translation (\( \alpha \)) is given by the following equation:

\[ \alpha(\lambda, R_{\text{protein}}) = \lambda \int_0^{\alpha} e^{-\lambda \Delta t} \left( \frac{\int_0^{\lambda (\Delta t, \lambda)} (\Psi(\Delta t, \lambda))^2 d\lambda}{\left( R_{\text{protein}} - \Delta r \right) / \lambda} \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \r...
Solid and dotted lines are the real and imaginary values of the eigenvalues in the Jacobian at equilibrium, respectively. SS, steady state. (of the genetic oscillator at different values of cation point around behaviour. In what follows, we analyse how circuits that build on nonlinear reactions to achieve optimal different values of impact on the nonlinear dynamics of the system. Therefore, translational (i.e. in the cytosol) dimerization, which, in turn, would tend to overlap more (i.e. higher values at equation (2.2)).

The results shown in figure 2 suggest that there is a fragile equilibrium in the fraction of co-translational versus post-translational (i.e. in the cytosol) dimerization, which, in turn, would impact on the nonlinear dynamics of the system. Therefore, different values of α will modify the performance of genetic circuits that build on nonlinear reactions to achieve optimal behaviour. In what follows, we analyse how α may be used to alter oscillations and bistability.

2.2. Case study: programmable nonlinearity in a genetic oscillator

A general requirement in order to obtain oscillations from a biological system is that its kinetic machinery must be ‘sufficiently nonlinear’ [44]. Here, we build a mathematical model for a theoretical three-component genetic oscillator, based on the ‘repressilator’ equations [45]. The model accounts for the new parameter that represents the fraction of dimerization that takes place during translation (α), and simulates how this parameter can, by itself, modify the nonlinearity of the system.

This genetic circuit is formed by a ring of repressors (proteins that negatively regulate a promoter), where each one regulates its successor (figure 3a). As a result, the concentration of all three proteins within the circuit oscillates in time. The system of ordinary differential equations (ODEs) that represents the oscillator is described as follows. Firstly, the ODE that calculates the concentration of monomeric repressors is

\[
\frac{dR_{i,\text{mono}}}{dt} = k_{\text{on}}(1 - \alpha)P_i - k_{\text{deg}}R_{i,\text{mono}} - k_{\text{dim}}R_{i,\text{dimer}}^2, \tag{2.4}
\]

where \(i \in \{1, 2, 3\}\) is a specific repressor protein, \(R_{\text{mono}}\) is the amount of repressor monomer in the cytosol (i.e. those monomeric regulators that did not dimerize during translation), \(k_{\text{on}}\) is the expression rate of monomers when the promoter \(P\) is not repressed (thus fully active), \(k_{\text{deg}}\) represents the degradation rate of monomers, \(k_{\text{dim}}\) is the rate of dimerization in the cytosol and \(\alpha\) is the fraction of monomers that become dimers during co-translation dimerization (which will dissolve as dimers in the cytosol). Therefore, equation (2.4) reads as follows: the concentration of monomers equals their production minus their degradation, and minus their consumption into dimerization.

Secondly, the ODE that calculates repressor dimers (i.e. the fully active protein) is given by

\[
\frac{dR_{\text{dimer}}}{dt} = k_{\text{on}}\alpha P_i - k_{\text{deg}} R_{i,\text{dimer}} + k_{\text{dim}} R_{i,\text{mono}}^2, \tag{2.5}
\]

where \(R_{\text{dimer}}\) is the dimerized repressor (note that in this model all three repressors of the system are assumed to be dimers in its final form). Lastly, the next ODE calculates the fraction of promoter \(P\) that is active (i.e. it is not being repressed by any R)

\[
\frac{dP_i}{dt} = k_{\text{un}}(1 - P_i) - \frac{1}{\tau_s} P_i R_{i-1,\text{dimer}}, \tag{2.6}
\]

where \(k_{\text{un}}\) is the unbinding rate of any dimer from its cognate promoter \(P\) and \(1/\tau_s\) is the binding rate of the same two components. Note that promoter number \(i\) is repressed by a repressor number \(i - 1\), where the previous element to \(i = 1\) is \(i = 3\), since the three genetic elements (1,2,3) are arranged in a ring.

Figure 3 shows how the parameter \(\alpha\) alters the nonlinear patterns of the system, to the point that the circuit stops oscillating if the balance between co- and post-translational dimerization is beyond a bifurcation point (figure 3b). That is, higher values of \(\alpha\) lead to a non-oscillating steady state.
This bifurcation, beyond which the oscillatory behaviour vanishes, is around $\alpha = 0.022$, which indicates that, even if the majority of dimers are formed in the cytosol, those that form during translation can drastically affect circuit behaviour. For the sake of comparison, the simulation where $\alpha = 0$ is equivalent to a model that does not consider this effect.

The new parameter $\alpha$ introduces complexity to the mathematical model in that it limits the range of parameter values that generate oscillations—it could be argued that it is more difficult to get reliable oscillations with it than without it. However, it offers several pathways to modify nonlinearity in vivo, unlike traditional methods for nonlinear dynamics (e.g. Hill coefficients). Therefore, its predictive scope narrows the gap that goes from modelling results to in vivo experimentation.

2.3. Case study: programmable nonlinearity in a genetic toggle switch

A genetic toggle switch [36] is a device built from two mutually inhibitory repressors that is able to flip between stable states (figure 4), in which only one of the two proteins is at high expression while the other one is inhibited. The stability of the system, and also the number of stable states, depends intricately on nonlinear dynamics. Although there are examples of genetic switches where nonlinearity emerges from protein dilution [46,47], the most common way of achieving nonlinear dynamics (and bistability) comes from transcription cooperativity—in which protein dimerization plays a fundamental role.

Our model for the toggle switch is specified by equations (2.6), (4.1) and (4.2), but with two (instead of three) repressor...
proteins (which are also assumed to be dimers). Furthermore, we added complexity to the model by considering the intra-cellular spatial distribution of genes, based on our recent work on spatio-temporal design [35,48]. This feature helps to differentiate between local and global repressors; that is, repressors that are in the proximity of, or far from, their encoding gene. The core message was that the distance a protein must ‘travel’ from its source gene to its target promoter modifies regulation in a predictable fashion. Since the differentiation between local and global proteins intersects with the model we introduce here, where proteins dimerize during translation (i.e. local) or in the cytosol during free diffusion (i.e. global), we analysed the genetic switch considering both dynamics.

Figure 4 shows the results of simulating the switch with two different spatial set-ups, proximity (figure 4a) and distance (figure 4b), and three values for the fraction of co-translational dimerization (α) in each case. Interestingly, the two spatial configurations show different performances for the same level of α, which implies that both phenomena (intergenic separation and protein dimerization) are closely connected in shaping nonlinear dynamics.

When the genes of the switch are placed in proximity (figure 4a), only a low value of α generates sufficient nonlinearity for the system to show bistability. This is because the generation of dimers imposed by co-translational dimerization is fully linear—so the fewer the better. As soon as this value increases, more dimerization takes place during translation, leading to a system malfunction; although the switching still occurs to some extent (e.g. α = 0.5), output values are low, and the intrinsic stochasticity of biological systems would result in unstable states. However, moving genes far apart (figure 4b) restored the function of the system, even in the case of α = 0.5 (a value we predict to be higher than physically plausible). By increasing the separation between the genes, the dimers formed near the source are not immediately available to bind to the target promoter, since this is now at a long distance. As a result, such a linear process is now less relevant: co-translated dimers must ‘travel’ from the source to the target, resulting in a decreased promoter-binding rate, which, in turn, removes its involvement in total promoter-binding events. Unlike the proximity scenario, where performance was only achieved at low values for α, the distance set-up showed bistability at any value. This highlights the role played by intra-cellular distance for circuit design. An extra simulation where α = 0 (i.e. the co-translational dimerization effect is not considered) can be found in the electronic supplementary material.

Altogether, simulations suggest that the necessary conditions for the emergence of bistability could be rationally designed or fine-tuned, and mapped into biological specifications such as ribosome binding sites (RBSs) (which impact on Δx) or intergenic separation.

3. Conclusion

The design of increasingly complex biological circuits in living cells is a major challenge. The lack of robust predictive modelling—which accurately foresees the performance of a design before implementation—threatens to undermine the success of the field. Although model-based design [49] is a common practice, accurate predictions are difficult to obtain since the internal workings of the cell are still based on unclear dynamics. Here, we focus on modelling protein dimerization [33] within regulatory interactions, as a way to predict and rationally design nonlinearity.

For protein dimerization to take place, monomers must meet within the internal milieu of the cell. Although there are previous efforts that highlight the relevance of this issue [38,39], the mathematical formalization of the mechanistic details responsible for dimerization has received little attention. Our model explicitly simulates co- and post-translational dimerization, which occur during and after translation, respectively. While the former imposes a linear regime on the reaction, the latter boosts the emergence of nonlinear dynamics. By controlling the fraction of each dimerization type, the model suggests routes for fine-tuning nonlinearity in vivo to fit pre-defined functional requirements. Moreover, the model was coupled to a previous model on spatio-temporal design that accounts for the diffusion of molecules within the volume of the cell [48]. Simulations suggested that intergenic distance (i.e. the physical distance between two inter-regulated genes) plays a fundamental role in shaping dimerization dynamics. Specifically, the linear dynamics imposed by co-translational dimerization are less important if the two interacting genes are far apart; and that distance can be adjusted in vivo by assigning different chromosomal locations to circuit components. Since nonlinear dynamics are at the core of biological [30] and computing [32] systems, their rational design would enable the construction of biological circuits with enhanced information-processing capabilities. The model presented here paves the way towards that goal.

Simulation results suggest a number of strategies on how to implement control over nonlinearity in vivo. For instance, (i) protein length [50] (adding tags or extra AAs), (ii) choice of RBS [51], since stronger RBSs will result in closer ribosomes on the mRNA, or (iii) ribosome availability [52] (influencing binding rates)—let alone the modification of intergenic distance [35]. Future work along this line will focus on obtaining experimental measurements of the impact of co-translation based on the aforementioned implementation strategies. These will result in identifying the extent to which nonlinear dynamics can be adjusted on-demand. Furthermore, future theoretical work will aim at studying whether co-translational oligomerization could be modelled with a similar approach. Our model accounts for first-order interactions (i.e. monomers with monomers) but many functional transcription factors are, in fact, dimers of dimers. While the model, as is, can simulate the post-translational dimerization of co-translated dimers (thus representing regulators such as LacI, which is a tetramer), it cannot describe the formation of oligomers during translation. Although it is unlikely to play a major role in nonlinearity, this possibility will be targeted in future research.

As precision is increasingly required from synthetic constructs, we advocate for the rational design of nonlinearity—a fundamental feature of biological systems. The model introduced here demonstrated the in-principle feasibility of it, and provides baseline information for future in vivo implementation.

4. Methods

4.1. Modelling the distance between ribosomes

In the model presented here, the distance between two consecutive ribosomes (Δx) is determined by (i) the rate of translation
and (ii) the difference in arrival time. This value is calculated as follows:

$$\Delta t = 3x_{bp}k_{\text{transl}}\Delta t,$$

where $x_{bp}$ is the width of a base pair, $ca$ 3 Å [53], and the factor of 3 comes from one AA being encoded by 3 bp.

This difference in arrival time ($\Delta t$) also leads to a difference in length ($\Delta r$) of partially translated proteins (or monomers). The calculation of the latter is captured by the next equation,

$$\Delta r = x_{AA}k_{\text{transl}}\Delta t,$$

where $x_{AA}$ is the width of a contour length of an AA, also $ca$ 3 Å [54].

The model assumes that this distance is constant until completing translation, which implies that the separation between ribosomes depends only on their binding times and not on sliding differences along the RNA.

4.2. Calculation of overlapping spheres

To calculate the overlap between the volumes of partially formed monomers we focus on a two-consecutive-ribosome scenario, which can be generalized to the ensemble of all ribosomes. In what follows, we show the derivation of equation (2.2) (i.e. overlapping fraction).

Here, we assume a system in which the two consecutive ribosomes have just initiated translation and are physically separated by a distance of $\Delta x$. The radii described by the partially formed monomers are $r_1$ and $r_2$, respectively. In this scenario, the spheres are then described by

$$x^2 + y^2 + z^2 \leq r_1^2 \quad (4.3)$$

$$x^2 + (y - \Delta x)^2 + z^2 \leq r_2^2.$$ \hspace{1cm} (4.4)

Using these equations, the edges of the spheres meet at a circle in the $yz$ plane at location $x$ determined by

$$y^2 + z^2 = r_1^2 - r_2^2 - (x - \Delta x)^2,$$ \hspace{1cm} (4.5)

which can be solved for $x^*$

$$x^* = \frac{\Delta x^2 + r_1^2 - r_2^2}{2\Delta x}.$$ \hspace{1cm} (4.6)

The overlapping volume can be described as a combination of two spherical domes; for visualization purposes, here we show the two-dimensional analogous circular segments. The value of $h$ is the height of the dome and $a$ is the radius of its disc.

where $a$ is the radius of the disc and $h$ is the height of the dome.

The value of $h$ differs between the two domes and is $r_1 - x^*$ and $r_2 - (\Delta x) + x^*$ for the ribosome at the origin and the ribosome shifted by $\Delta x$, respectively. Assuming that the translation rate is constant, the length of the transcripts of consecutive ribosomes is $r_1 = r$ and $r_2 = r + \Delta r$, with $\Delta x$ as determined by equation (4.2). The ribosome arrival time also determines the distance between the ribosomes ($\Delta r$) via equation (4.1).

Data accessibility. All time simulations, bifurcation analyses, derivations and data visualization were done in Wolfram Mathematica 12.0. Notebooks are available at https://github.com/ rstoofo/TranslationMediatedDimerisation.

Authors’ contributions. R.S. and Á.G.-M. designed the research. R.S. developed the model and performed simulations. Both authors interpreted the results and Á.G.-M. wrote the manuscript.

Competing interests. We declare we have no competing interests.

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