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How can infectious medical waste be forecasted and transported during the COVID-19 pandemic? A hybrid two-stage method

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ABSTRACT

The COVID-19 pandemic has caused an unforeseen collapse of infectious medical waste (IMW) and an abrupt smite of the conveying chain. Hospitals and related treatment centers face great challenges during the pandemic because mismanagement may lead to more severe life threats and enlarge environmental pollution. Opportune forecasting and transportation route optimization, therefore, are crucial to coping with social stress meritoriously. All related hospitals and medical waste treatment centers (MWTCs) should make decisions in perspective to reduce the economic pressure and infection risk immensely. This study proposes a hybrid dynamic method, as follows: first to forecast confirmed cases via infectious disease modeling and analyze the association between IMW outflows and cases; next to construct a model through time-varying factors and the lagging factor to predict the waste quantity; and then to optimize the transportation network route from hospitals to MWTCs. For demonstration intentions, the established methodology is employed to an illustrative example. Based on the obtained results, in finding the process of decision making, cost becomes the common concern of decision-makers. Actually, the infection risk among publics has to be considered simultaneously. Therefore, realizing early warning and safe waste management has an immensely positive effect on epidemic stabilization and lifetime health.

1. Introduction

Due to the infectious characteristic of the COVID-19 pandemic, social deaths from the virus have been higher than in past years (Jacobson and Jokela, 2021). In addition to the high death toll, the ongoing COVID-19 pandemic has, since its global concern in late 2019, led to social disorders, changes in lifestyle habits and environmental pollution (Wenham et al., 2021). A high-risk infectious rate, a large number of patients and large-scale spread paths have always been typical features of COVID-19. The coronavirus propagates easily via respiratory droplets, close contact and aerosols. Meanwhile, the explosive demand for medical materials and related services has caused a massive rise in the waste generation rate (Kargar et al., 2020). Virus-contaminated infectious medical waste (IMW), such as masks, protective clothing, pharmaceutical packaging and domestic waste, is generated in the process of prevention, control, treatment and recovery, with various potential risks to humans (Hantoko et al., 2021). The peak daily IMW produced in Wuhan City, the epicenter of China, reached 247 tons by 1 March 2020, which is a 5- to 6-fold increase from between 40 and 50 tons (You et al., 2020). Accurate forecasting and reasonable waste transportation will help reduce infectious risk and build an environmental-friendly atmosphere.

All of these special considerations, sudden breakouts, rare occurrences and global scopes, place limitations on the practicality of forecasting waste quantity during the COVID-19 outbreak as urgent social issues. Many previous papers in the waste forecasting field have focused on other types of waste, such as household waste, electronic waste, construction and demolition waste (Song et al., 2017; Althaf et al., 2019; Sunayana et al., 2021; Wang et al., 2021; Johnson et al., 2017). The methods involved in these studies may be listed into several categories: grey model (GM), support vector regression (SVR), logistics forecasting models, nonlinear autoregressive (NAR) models, variational mode decomposition (VMD), exponential smoothing model (ESM) and gradient boosting models. There was one respect, however, in which these modeling methodologies rely on sufficient existing data and have their own disadvantages.

Due to the particularity of infectious medical waste during the epidemic, which is different from general waste, the main difficulty of the existing method is that it cannot be proven correct for its application...
in the epidemic. Some researchers proposed that the quantity of healthcare hazards is proportional to the confirmed cases, and further, there is informative information about the association between IMW outflows and diagnosed cases as well as a special lagged relationship (Richter et al., 2021). Some authors offered constructive insights to predict COVID-19 trends and patients, which may support more directional and targeted approaches to be provided, so as to forecast the number of IMW in other perspectives. A multi-logistic model method (Devezas and Miranda, 2021) is applied to predict the trend of the COVID-19 pandemic. Furthermore, infectious disease models are used extensively for real-time epidemic forecasting, particularly in the case of COVID-19. Rezapour et al. (Rezapour et al., 2020) modified the susceptible–exposed–infected–recovered (SEIR) model for the transmission of COVID-19 by the Caputo fractional derivative. Pokharel et al. (Pokharel et al., 2021) provided a novel agent based simulation (ABS) model using the SEIR framework to evaluate the effectiveness of manual contact tracing compared to bulletin board contact tracing under COVID-19. Shou et al. (Shou et al., 2021) combined a SEIR epidemic model with non-pharmaceutical interventions to analyze the number of COVID-19. Pokharel et al. (Pokharel et al., 2021) provided a novel agent based simulation (ABS) model with non-pharmaceutical interventions to analyze the number of infected patients under different conditions. Annas et al. (Annas et al., 2020) considered isolation and vaccination factors and obtained the basic reproduction numbers of the SEIR model via the generation matrix method. Considering the abundant literature on the SEIR model and the correlation between IMW outflows and diagnosed cases for some time yet, the contributions of the proposed prediction method may be extremely meaningful for the medical and cleaning industry.

Aside from this, appropriate waste management is also crucial to health and safety at all times, let along during the COVID-19 pandemic (Richter et al., 2021). Multi-criteria decision making (MCDM) methods are broadly applied to the process of medical waste management, especially in seeking results regarding management techniques, disposal methods and processing sites aspects (Xiao, 2018; Aung et al., 2019; Dursun et al., 2011; Liu et al., 2013; Narayananmooorthy et al., 2020; Manupati et al., 2021). Although Analytic Hierarchy Process (AHP), Technique for Order Preference by Similarity to Ideal Solution (TOPSIS), VIKOR, fuzzy set theory, grey theory and other decision-making methods are involved in the above researches, the decision-makers are generally considered to be absolutely rational when facing risk. This study singles out the details, which have been neglected in existing relevant studies, and enriches the theories and methods by exploring the bounded rationality from IMW management during COVID-19.

Along with the works listed above, optimization has been actively employed for medical waste collection (Vu et al., 2019; Mantzarakas and Voudrias, 2017) and treatment to lessen environmental influences and socioeconomic pressure. Yao et al. (Yao et al., 2019) provided a soft-path solution to meet the medical waste disposal demand in optimal medical waste disposal center sites. And Taslimi et al. (Taslimi et al., 2020) presented a Periodic Load-dependent Capacitated Vehicle Routing Problem (PLCVRP) for the plan of a weekly inventory routing arrangement to carry medical waste to treatment locations. All of the above considered social cost and management risk in the route optimization, which allow us to solve IMW transportation challenges and select medical waste treatment centers (MWTCs) better during COVID-19.

There are growing policy recommendations to cope with severe stress that have arisen with the epidemiological trend. Large quantities of IMW require desperate forecasting and transportation, and both are important to environmental safety and socioeconomics, which are useful to reduce the pressure on hospitals and MWTCs. In response to the ongoing COVID-19 crisis, the United Nations Industrial Development Organization supports medical waste management efforts around the world.

This paper proposes a hybrid two-stage method to achieve accurate prediction and transportation route optimization based on the contributions and deficiencies of existing articles. The remainder of the paper is structured as follows: Section 2 presents a brief introduction to preliminaries. Section 3 proposes the hybrid two-stage method. Section 4 gives a case study to demonstrate the practicability of the presented methodology. Finally, the conclusions are made in Section 5.

2. Preliminaries

This section briefly introduces some basic concepts regarding triangular fuzzy numbers (TFNs), linguistic term sets, and cumulative prospect theory (CPT), which provides a basis for this article.

2.1. Triangular fuzzy numbers and linguistic term sets

TFNs are proposed to solve the problem in an uncertain environment and have an excellent ability to guarantee the completeness of decision information. In this section, we introduce TFNs to describe the language information of experts.

Definition 1. The fuzzy number \( \tilde{u} \) is a TFN, and its membership function is expressed as follows by the mathematical method:

\[
\tilde{u}(x) = \begin{cases} 
0 & \text{if } x < \bar{u} \\
\frac{(x - \bar{u})}{(\bar{u} - \underline{u})} & \text{if } \bar{u} \leq x \leq u \\
\frac{u - x}{u - \underline{u}} & \text{if } u \leq x \leq \overline{u} \\
0 & \text{if } x > \overline{u}
\end{cases}
\]

where \( \underline{u} \) and \( \overline{u} \) are the lower and upper limits of the fuzzy number, and \( u \) is the most likely value, then the TFN is expressed as \( \tilde{u} = (u, \underline{u}, \overline{u}) \).

Definition 2. Let \( \tilde{u} = (u, \underline{u}, \overline{u}) \) be a TFN, and the defuzzification value is as follows (Chang, 1996):

\[
D(\tilde{u}) = \left( u + 4\underline{u} + \overline{u} \right) / 6
\]

Definition 3. The Euclidean distance can be used to describe the difference value between \( \tilde{u}_1 = (u_1, \underline{u}_1, \overline{u}_1) \) and \( \tilde{u}_2 = (u_2, \underline{u}_2, \overline{u}_2) \):

\[
d(\tilde{u}_1, \tilde{u}_2) = \sqrt{\left( (u_1 - u_2)^2 + (\underline{u}_1 - \underline{u}_2)^2 + (\overline{u}_1 - \overline{u}_2)^2 \right) / 3}
\]

To realize the transformation between linguistic terms and TFNs, it is necessary to determine the relationship mapping. Let \( S = \{S_0, S_1, \ldots, S_T\} \) be a fully ordered linguistic item set with an odd number of bases, where \( S_t \) is the \( t+1 \)-th language term and \( T+1 \) is the base of \( S \). It proposed a method to represent the multi-granularity linguistic information by fuzzy numbers (Jiang et al., 2008).

\[
\tilde{u} = (u, \underline{u}, \overline{u}) = (\max((t-1)/T, 0), t/2, \min((t+1)/T, 1)) \cdot t = 0, 1, \ldots, T
\]

2.2. Cumulative prospect theory

Tversky and Kahneman (Tversky and Kahneman, 1992) proposed CPT, which was developed by prospect theory and expected utility theory. It includes q experts \( (E_1, E_2, \ldots, E_q) \) and n alternatives \( (A_1, A_2, \ldots, A_n) \) as well as m criteria \( (C_1, C_2, \ldots, C_m) \). As one of the influential behavior decision theories, CPT considers both the psychology and the behavior of decision-makers under risk. It has been increasingly used in abundant and extensive decision-making fields.

It proposed a value function to represent the risk preference, which is described by Eq. (5).

\[
\begin{align*}
\psi^+_{\lambda}(x) &= (1 - \lambda) x + \lambda x^a \\
\psi^-_{\lambda}(x) &= -\lambda(1 - \lambda) x + \lambda x^b
\end{align*}
\]

where \( \lambda \) is the coefficient of risk aversion, which indicates that decision-makers are more sensitive to losses than to gains, \( \lambda > 1 \); and \( x < 0 \) represents losses, \( x \geq 0 \) represents the gains; \( a \) and \( \beta \) are two index

parameters that are relevant to gains and losses, respectively, \( 0 \leq \alpha \leq \beta \leq 1 \). According to the previous experiments (Tversky and Kahneman, 1992), we suppose the values of these parameters are \( \alpha = \beta = 0.88 \) and \( \delta = 2.25 \).

As shown in Eq. (6), the weight function was described. The value function shows that decision-makers are inclined to overrate small probability events while underestimating high and medium possibility events.

\[
\begin{align*}
\pi^+(\omega) &= (\omega_0)^{\gamma} / \left( (\omega_0)^{\gamma} + (1 - \omega_0)^{\gamma} \right)^{1/\gamma} \\
\pi^-(\omega) &= (\omega_0)^{\delta} / \left( (\omega_0)^{\delta} + (1 - \omega_0)^{\delta} \right)^{1/\delta}
\end{align*}
\]

where \( \gamma \) and \( \delta \) indicate the attitude of decision-makers toward gains and losses, respectively, \( \gamma = 0.61, \delta = 0.69 \); \( \pi^+(\omega_0) \) and \( \pi^-(\omega_0) \) are the weight functions.

The cumulative prospect value \( V_i \) can be obtained as follows:

\[
V_i = \sum_{j=1}^{m} v_j^+ \pi^+(\omega_j) + \sum_{j=1}^{m} v_j^- \pi^-(\omega_j)
\]

### 3. Problem description

This section gives a detailed description of the proposed hybrid two-stage model and a resolution framework. Moreover, the notations are defined to describe the variables and sets.

#### 3.1. Problem description and resolution framework

During the epidemic outbreak, there was a surplus of infectious medical waste, which may have resulted in a higher virus risk of individual exposure. Therefore, hospitals first have to collect and transport medical waste to MWTCs. Additionally, MWTCs are supposed to dispose of medical waste quickly. If we can develop a new approach to better predict the amount of medical waste, hospitals and MWTCs may better handle the epidemic. First, the two-stage method proposes a time evolution prediction model to predict the daily waste quantity. Second, with the goal of reducing the total social cost and the infection risk, this paper builds the multi-objective model to realize the optimization of transportation routes and select the appropriate MWTCs for hospitals. Put together, the resolution framework is drawn in Fig. 1.

### 3.2. Notations

The mathematical symbols used in the model are explained as follows:

- \( h \) is the subscript of the point of hospitals, \( h = 1, 2, \ldots, H \); \( t \) is the subscript of the point of MWTCs, \( t = 1, 2, \ldots, T \);
- \( W_h \) is the amount of waste generated by the hospital \( h \) that is equivalent to the volume initially disinfection by the hospital \( h \);
- \( F_h \) is the fixed cost of disinfection in the hospital \( h \);
- \( M_h \) is the unit disinfection cost in the hospital \( h \);
- \( F_{ht} \) is the fixed cost of transporting IMW from the hospital \( h \) to the treatment center \( t \);
- \( M_{ht} \) is the unit cost of transporting IMW from the hospital \( h \) to the treatment center \( t \);
- \( L_{ht} \) is the distance from the hospital \( h \) to the treatment center \( t \);
- \( F_t \) is the fixed disposal cost of IMW in the waste treatment center \( t \);
- \( M_t \) is the unit disposal cost of IMW in the treatment center \( t \).

### 4. The hybrid two-stage method

#### 4.1. Stage 1: predicting the quantity of infectious medical waste

Predicting the waste quantity involves two major steps: (1) In addition to considering quarantine measures and asymptomatic infected individuals, this paper introduces the effect of exposed individuals on susceptible people and thus establishes an improved SEIR model. This includes selecting an appropriate infectious disease model and then improving it according to the actual situation; (2) Establishing a time evolution prediction model. This step proposes a new function to predict the daily waste quantity accurately based on the confirmed cases and the lagged relationship.

#### 4.1.1. Determining the modified SEIR model

This paper revises the existing dynamic models of epidemic transmission (Tang et al., 2020). Because exposed individuals can transmit risk and asymptomatic infected individuals are infectious but not easily identifiable, we describe the compartments and redefine the interaction...
relationship between different populations. It covers susceptible (S), exposed (E), infectious (I) and recovered (R) populations in the classic SEIR model. Considering the actual scenario of COVID-19, infectious people fall into two categories: symptomatic (I) and asymptomatic (I') infected individuals. Considering quarantine measures against infectious diseases, the compartments are further refined as isolated susceptible (S'), isolated exposed (E') and isolated infectious (I'). Given the circumstances, I' will be immediately sent to designated hospitals for isolation and treatment, so they are all transformed into hospitalized patients (H). Therefore, S, E, I, and L refer to susceptible, exposed, symptomatic and asymptomatic persons missed in isolation, respectively. The transformation relationship is shown in Fig. 2. The model assumes that all people can be infected. Quarantined susceptible individuals are transferred back to susceptible people after being released from quarantine. Both infectious and exposed populations have different degrees of ability to infect susceptible people and then turn them into exposed individuals.

The differential equations in Eq. (8) can describe the modified SEIR model.

\[
dS/dt = -[\rho c(1-\beta') + \rho c \beta' + \rho c(1-i)\beta']S(I_t + \tau_1E + \tau_2I_t) + rS,
\]

\[
dE/dt = [\rho c(1-\beta') - S(I_t + \tau_1E + \tau_2I_t)] - \alpha E,
\]

\[
dI'/dt = \alpha (1-b)E - \omega I_s,
\]

\[
dS'/dt = [\rho c(1-i)\beta']S(I_t + \tau_1E + \tau_2I_t) - \alpha E,
\]

\[
dE'/dt = \rho c \beta' S(I_t + \tau_1E + \tau_2I_t) - \mu E_i,
\]

\[
dI''/dt = \mu I_s + \mu E_i - (d + \omega)h,
\]

\[
dR/dt = I_{0s} + I_{0r} + H_{0h},
\]

where \( i \) is the isolation ratio; \( \beta' \) is the transmission probability; \( c \) is the contact rate; \( \rho \) is the effective contact coefficient; \( \alpha \) is the conversion ratio of exposed people to infectious people. Because the average latency period of the early hypothesis is seven days, the value of \( \alpha \) is 1/7; \( r \) is the rate of isolation release. So \( r \) is equal to 1/14, considering that the average isolation period is 14 days; \( b \) is the proportion of individuals with symptoms; \( \mu_i \) is the rate at which infectious people with symptoms turn into isolated infectious people; \( \mu_i \) is the rate at which isolated exposed people turn into isolated infectious people; \( \omega_a \) is the rate at which asymptomatic infected people convert to recovered people; \( \omega_h \) is the rate at which inpatients convert to recovered people; \( d \) is the death rate; \( \tau_1 \) is the infection intensity in the exposed people compared to symptomatic infected people; \( \tau_2 \) is the infection intensity in the asymptomatic infected people compared to symptomatic infected people. Consider \( i, \beta, c, b, \mu_i, \mu_i, \omega_a, \omega_h, d > 0 \), and \( \tau_1 = \tau_2 = 1 \).

4.1.2. Establishing the time evolution prediction model

The next step is to establish the prediction function of IMW quantity based on the SEIR model. Predicting waste quantity has been studied in various methods, such as machine learning, neural networks, support vector machines, etc., but all of these need to be built on massive historical data. Although some researchers advised predicting IMW quantity based on the SEIR model, but it did not give a specific modeling method.

To compensate for these deficiencies, this paper proposes the following linear time-varying function between the waste quantity and the SEIR model at time \( t \):

\[
W_t = \pi \epsilon H(t)
\]

where \( W_t \) refers to the waste quantity at time \( t \), and \( \epsilon \) is the ratio coefficient, which corresponds to the volume of IMW per infected person per day; \( \pi \) is the waste volume correction factor and \( H(t) \) is the number of existing confirmed patients at time \( t \). As much waste as there is demand. Liu and Xiao (Liu and Xiao, 2015) described the relationship between healthcare demand and the number of people infected, and we further transform and improve the relationship. Considering the short supply in the early stage of the epidemic, the waste quantity is less than the demand. The supply and demand are matched in the middle and late stages, and then the waste quantity and demand reach an equilibrium state, so the early stage \( \pi < 1 \) and the later stage \( \pi = 1 \).

Nevertheless, the influence of early medical supplies on material demand in later stages should be considered in the linear relationship. For example, if the amount of medical waste at cycle \( t \) is \( W_t^* \), the number at cycle \( t-1 \) would have been \( W_{t-1}^* \) according to Eq. (9). However, the medical materials in decision cycle \( t \) will have a positive impact on \( t+1 \), which will change the waste quantity of cycle \( t+1 \) to \( W_{t+1}^* \) instead of \( W_{t+1}^* - x \), and \( x \) is the lagging effect. Hence, the expected volume at cycle \( t+1 \) should be \( W_{t+1}^* \) instead of \( W_{t+1}^* \). The lagging factor is introduced to describe the lagging effect:

\[
\chi_t = \frac{W_{t+1}^* - W_t}{W_t^*}
\]

Here, the lagging factor \( \chi_t \) can be either increasing volume or decreasing volume and may change with medical materials at cycle \( t \). For an infected person, there are only two states of transition: recovery or death. No matter which one they become, they no longer have the possibility to infect others. In other words, the virus is effectively blocked in this case. We denote the blocking rate as \( \theta \) and the cure cycle as \( \sigma \), which is an integer multiple of the decision-making cycle, then the blocking rate of each cycle can be described as \( \theta/\sigma \). Such a hypothesis would reasonable because the decision-making cycle is small enough (one day). Therefore, we get the recurrence Eq. (11).

\[
W_t = \pi \epsilon H(1) \text{ is the initial waste volume, and } H(1) \text{ is the initial number of confirmed cases. Eq. (11) is the defined time evolution prediction model for the quantity of IMW.}
\]

\[
t = 1: W_1 = \pi \epsilon H(1)
\]

\[
t = 2: W_2 = (1 + \chi_1) \left( 1 - \frac{\theta}{\sigma} \right) W_1
\]

\[
t = 3: W_3 = (1 + \chi_2) \left( 1 - \frac{\theta}{\sigma} \right) W_2
\]

\[
= (1 + \chi_1) (1 + \chi_2) \left( 1 - \frac{\theta}{\sigma} \right) W_1
\]

\[
\cdots
\]

\[
t = n: W_n = \prod_{t=1}^{n} (1 + \chi_t) \left( 1 - \frac{\theta}{\sigma} \right)^{n-1} W_1
\]

4.2. Stage 2: a multi-objective optimization model for the transportation route of infectious medical waste

The discharge of IMW will surge in a short period of time, and the limited area within hospitals cannot meet the preservation demand, so it needs to be transferred to MWTCs as soon as possible. It is important to assess the anti-risk capability of MWTCs to help hospitals choose the right one for waste disposal and thus reduce the infection risk.
Meanwhile, reducing the total cost can relieve socioeconomic stress. The transportation network route of IMW involves three major steps: (1) Adopting the CPT to assess the anti-risk capability of MWTCs. (2) Establishing a cost optimization function to relieve socioeconomic stress. (3) Based on the cost function and anti-risk capability evaluation results, the multi-objective optimization model is established, and the appropriate MWTC is selected to realize the optimization of the transportation route.

4.2.1. Assessing the anti-risk capability of treatment centers

Step 1 Determine the positive and negative reference points

Choosing the right reference point is vital when we employ CPT. Generally speaking, reference points should be selected from some representative points, such as zero value, average value, peak value and least value. Referring to the idea of the TOPSIS method, we choose the representative points, such as zero value, average value, peak value and least value. Referring to the idea of the TOPSIS method, we choose the representative points, such as zero value, average value, peak value and least value. Referring to the idea of the TOPSIS method, we choose the representative points, such as zero value, average value, peak value and least value.

Step 2 Calculate gains and losses

Let \( G_j \) be the gains, and \( L_j \) be the losses. The distance between each alternative and \( R_j^+ / R_j^- \) is calculated using Eq. (3), which is the \( L_j / G_j \).

Step 3 Compute the positive and negative prospect value matrices of gains and losses

Computing the positive and negative prospect value matrices \( V_{ij}^+ \) and \( V_{ij}^- \) via Eq. (5).

Step 4 Determine the cumulative prospect weights

Eq. (6) is used to determine the cumulative prospect weights.

Step 5 Gain the cumulative prospect values

Calculating the cumulative prospect value \( V_t \) for each alternative via Eq. (7).

4.2.2. Establishing the cost optimization function

Because infectious medical materials are different from the other types, hospitals should first perform preliminary sterilizing work to reduce the infection risk during the transport and disposal process. There are various costs involved in the whole process, such as transportation cost, sterilization cost, disposal cost, etc. We have to consider how to optimize the waste transportation route to minimize the costs of the whole process.

According to the actual situation, the following assumptions are made:

(i) Hospitals have enough space to store the clinical waste generated each day and can establish primary sites for health-infection;
(ii) The roads between hospitals and treatment centers are interconnected, and the waste can be successfully transported to the centers;
(iii) Each treatment center can handle all kinds of IMW, such as discarded protective clothing, masks, contaminated instruments, etc.

The cost optimization model based on the transportation network of hospitals and MWTCs is established as follows:

\[
\min Z_t = \sum_{h \in H} (F_h + W_h M_h) + \sum_{h \in H} \sum_{t \in T} (\eta_h E_{ht} + \eta_h L_{ht} W_h M_h) + \sum_{h \in H} \sum_{t \in T} (F_t + W_t M_t)
\]  

(12)

Eq. (12) is the optimization model for minimizing costs, including the disinfection, transportation and disposal costs. \( W_h \) is the volume of waste transported from hospital \( h \) to treatment center \( t \). \( \eta_h \) is the binary variable that decides if there is IMW transported from hospital \( h \) to the disinfection, transportation and disposal costs. \( \eta_h \) denotes the fixed and unit transportation costs from hospitals to MWTCs. The fixed and unit transportation costs from hospitals to MWTCs.

4.3. Building and solving the multi-objective optimization model

It is assumed that the cumulative prospect value of treatment center \( t \) is \( U(D_t) \), so we can establish the multi-objective optimization model as follows:

\[
\min Z_t = \sum_{h \in H} (F_h + W_h M_h) + \sum_{h \in H} \sum_{t \in T} (\eta_h E_{ht} + \eta_h L_{ht} W_h M_h) + \sum_{h \in H} \sum_{t \in T} (F_t + W_t M_t)
\]

(13)

\[
\max Z_t = \sum_{h \in H} U(D_t) \eta_h
\]

(14)

Constraints:

\[
\sum_{h \in H} W_h \leq \sum_{h \in H} W_h, \forall h \in H
\]

(15)

\[
W_h \geq 0, \forall h, t \in T
\]

(16)

\[
W_t \leq \text{Cap}_W, \forall t \in T
\]

(17)

\[
W_t \geq 0, \forall h \in H, \forall t \in T
\]

(18)

\[
\eta_h \in \{0, 1\}, \forall h \in H, \forall t \in T
\]

(19)

\[
\eta_h \in \{0, 1\}, \forall h \in H, \forall t \in T
\]

(20)

\[
\phi(Z_t) = \frac{Z^\max_t - Z_t}{Z^\max_t - Z^\min_t}
\]

(22)

\[
\phi(Z_t) = \frac{Z^\max_t - Z_t}{Z^\max_t - Z^\min_t}
\]

(23)

Assuming that the weight coefficients of functions \( \phi(Z_1) \) and \( \phi(Z_2) \) are \( k_1 \) and \( k_2 \), respectively, and thus the multi-objective optimization model can be transformed into a single-objective model via the linear weighting method, which can be expressed as follows:

\[
\max Z_t = k_1 \phi(Z_1) + k_2 \phi(Z_2)
\]

(24)

Finally, Eq. (24) can be solved by intelligent optimization algorithms or optimizing software packages.

5. Illustrative example

5.1. Background

COVID-19 has been rapidly spreading worldwide since December 2019, with a massive surge of infections in a short period, followed by a...
large amount of medical waste. The waste quantity is closely related to the number of confirmed cases, and the SEIR model-based methods for predicting epidemic diseases have been relatively mature. This paper assumed that COVID-19 was spreading in W city, and the infectious medical waste during the outbreak period was predicted and treated. There are not many centers dedicated to IMW, and the existing MWTCs are unable to meet the treatment needs. In this case, it is necessary to transform general waste treatment centers or to build specialized MWTCs. Special-T Environmental Engineering Co., Ltd. is the only medical waste treatment company. Forced by the grim situation, with the Ministry of Ecology and Environment’s support, the Environmental Protection Bureau transformed W’s most significant industrial waste treatment plant, Reconstructed-T Environmental Protection Technology Co., Ltd., to help dispose of some medical waste. Meanwhile, W city builds the NewB-T Medical Waste Disposal Center, an emergency MWTC with a daily capacity of 30 tons, within half a month. As many as 40 treatment institutions are receiving COVID-19 patients, which can accommodate 13,605 patients. W-one Hospital, W-two Hospital and W-three Hospital are the most representative hospitals that can treat 1000, 1500, 720 patients, respectively. According to the total amount of waste predicted, the daily waste quantity of each hospital can be calculated.

5.2. Data generation

Based on existing literature (Tang et al., 2020) and the empirical situation, the parameters’ values of the improved SEIR model are shown in Table 1.

| Parameter | Definitions | Value |
|-----------|-------------|-------|
| $\alpha$  | Isolation ratio | $1.8887 \times 10^{-7}$ |
| $\beta$   | Transmission probability | $2.1011 \times 10^{-8}$ |
| $c$       | Contact rate | 2 |
| $\rho$    | Effective contact coefficient | 0.8 |
| $\sigma$  | The proportion conversion ratio of exposed people to infectious people | 1/7 |
| $\tau$    | The rate of isolation release | 1/14 |
| $b$       | The proportion of people with symptoms | 0.86834 |
| $\mu_1$   | The rate at which infectious people with symptoms turn into isolated infectious people | 0.13266 |
| $\mu_2$   | The rate at which isolated exposed people turn into isolated infectious people | 0.1259 |
| $\nu_1$   | The rate at which asymptomatic infected people convert to recovered people | 0.13978 |
| $\nu_2$   | The rate at which symptomatic infected people convert to recovered people | 0.33029 |
| $\nu_3$   | The rate at which inpatients convert to recovered people | 0.46634 |
| $d$       | Death rate | $1.7826 \times 10^{-5}$ |
| $\gamma_1$ | The infection intensity in the exposed people compared to symptomatic infected people | 1 |
| $\gamma_2$ | The infection intensity in the asymptomatic infected people compared to symptomatic infected people | 1 |

Table 1

Parameters’ values of the improved SEIR model.

| Initial values | Definitions | Value |
|----------------|-------------|-------|
| $S(0)$         | Initially unisolated susceptible individuals | 11,081,000 |
| $R(0)$         | Initially unisolated exposed individuals | 105.1 |
| $I(0)$         | Initially asymptomatic infected individuals | 53.839 |
| $E(0)$         | Initially symptomatic infected individuals | 27.679 |
| $H(0)$         | Initially isolated recovered individuals | 2 |
| $I(0)$         | Initially isolated susceptible individuals | 739 |
| $E(0)$         | Initially isolated exposed individuals | 1.1642 |
| $H(0)$         | Initially hospitalized patients | 1 |

Table 2

Cost-related parameters.

| Treatment centers | Fixed operating cost (¥) | Unit treatment cost (¥/kg) |
|-------------------|-------------------------|---------------------------|
| Special-T         | 390,000                 | 0.900                     |
| Reconstructed-T   | 380,000                 | 1.000                     |
| NewB-T            | 400,000                 | 0.800                     |

| Treatment centers | Fixed transport cost (¥) | Unit transport cost (¥/kg/km) | Capacity (kg/day) |
|-------------------|-------------------------|-------------------------------|------------------|
| Special-T         | 1500                    | 0.035                         | 20,000           |
| Reconstructed-T   | 2000                    | 0.040                         | 30,000           |
| NewB-T            | 1750                    | 0.050                         | 50,000           |

| Hospitals | Fixed cost (¥) | Unit “health infected” cost (¥/kg) |
|-----------|----------------|-----------------------------------|
| W-one     | 3000           | 0.065                             |
| W-two     | 2000           | 0.060                             |
| W-three   | 2000           | 0.060                             |

| Distance   | W-one | W-two | W-three |
|------------|-------|-------|---------|
| Special-T  | 7.7 km | 40 km | 50 km   |
| Reconstructed-T | 28 km | 84 km | 19 km   |
| NewB-T     | 31 km | 41 km | 41 km   |

5.3. Results

Based on Eq. (8)-Eq. (11) and the obtained data, the results are calculated.

For the criteria of five experts are gathered and concentrated by the weighted average operator. Then, the decision matrix expressed by TFNs can be received, as given in Table 3.

The defuzzification values are calculated according to the decision
The decision matrix represented by TFNs.

| Experts | Criteria | Treatment centers | Reconstructed-T | NewB-T |
|---------|----------|------------------|----------------|--------|
| Expert 1 | Experience and qualification (C1) | (0.75,1,1) | (0.5,0.75,1) | (0.25,0.5,0.75) |
|         | Equipment and technology (C2) | (0.5,0.75,1) | (0.25,0.5,0.75) | (0.75,1,1) |
|         | Waste disposal site exposure to public (C3) | (0.25,0.25,0.5) | (0.25,0.5,0.75) | (0.25,0.5,0.75) |
|         | Area covered by HCW disposed (C4) | (0.25,0.5,0.75) | (0.25,0.5,0.75) | (0.75,1,1) |
|         | Release with health effects (C5) | (0.75,1,1) | (0.5,0.75,1) | (0.25,0.5,0.75) |
|         | Instance from urban area (C6) | (0.25,0.25,0.5) | (0.25,0.5,0.75) | (0.75,1,1) |
|         | Probability of infection (C7) | (0.25,0.25,0.5) | (0.25,0.5,0.75) | (0.75,1,1) |
| Expert 2 | Experience and qualification (C1) | (0.75,1,1) | (0.5,0.75,1) | (0.5,0.75,1) |
|         | Equipment and technology (C2) | (0.75,1,1) | (0.5,0.75,1) | (0.75,1,1) |
|         | Waste disposal site exposure to public (C3) | (0.5,0.75,1) | (0.5,0.75,1) | (0.75,1,1) |
|         | Area covered by HCW disposed (C4) | (0.25,0.5,0.75) | (0.25,0.5,0.75) | (0.75,1,1) |
|         | Release with health effects (C5) | (0.25,0.5,0.75) | (0.25,0.5,0.75) | (0.75,1,1) |
|         | Instance from urban area (C6) | (0.25,0.5,0.75) | (0.25,0.5,0.75) | (0.75,1,1) |
|         | Probability of infection (C7) | (0.25,0.5,0.75) | (0.25,0.5,0.75) | (0.75,1,1) |
| Expert 3 | Experience and qualification (C1) | (0.75,1,1) | (0.75,1,1) | (0.5,0.75,1) |
|         | Equipment and technology (C2) | (0.75,1,1) | (0.75,1,1) | (0.5,0.75,1) |
|         | Waste disposal site exposure to public (C3) | (0.5,0.75,1) | (0.5,0.75,1) | (0.75,1,1) |
|         | Area covered by HCW disposed (C4) | (0.25,0.5,0.75) | (0.25,0.5,0.75) | (0.75,1,1) |
|         | Release with health effects (C5) | (0.25,0.5,0.75) | (0.25,0.5,0.75) | (0.75,1,1) |
|         | Instance from urban area (C6) | (0.25,0.5,0.75) | (0.25,0.5,0.75) | (0.75,1,1) |
|         | Probability of infection (C7) | (0.25,0.5,0.75) | (0.25,0.5,0.75) | (0.75,1,1) |

Matrix $[\bar{R}]_{ij}$ and Eq. (2). After that, the reference points of every MWTC under each criterion are described as follows:

$$R_i = \left\{ R_1^i, R_2^i, \ldots, R_e^i \right\}$$

$$G_i = \begin{bmatrix} d\left(A_1, R_1^i \right) \\
\vdots \\
\vdots \\
\vdots \\
d\left(A_e, R_e^i \right) 
\end{bmatrix}$$

$$L_i = -\begin{bmatrix} d\left(A_1, R_1^i \right) \\
\vdots \\
\vdots \\
\vdots \\
d\left(A_e, R_e^i \right) 
\end{bmatrix}$$

$$[\bar{R}]_{ij} = \left\{ \min_{I \in \mathbb{G}_A} (\bar{u}_I), \max_{I \in \mathbb{G}_A} (\bar{u}_I), \ldots, \max_{I \in \mathbb{G}_A} (\bar{u}_m) \right\}$$

After obtaining the gain and loss values, we can determine the prospect values $V_i$ and $V_j$ by Eq. (5).
Based on judgments about expert consensus, the weights of criteria are obtained, $\omega_i = (0.1, 0.1, 0.15, 0.05, 0.25, 0.05, 0.3)$. The cumulative prospect weights can be expressed as follows:

$$\pi^+(\omega) = [0.1863\ 0.2269\ 0.1316\ 0.2907\ 0.1316\ 0.3184]$$

$$\pi^-(\omega) = [0.1701\ 0.1701\ 0.2167\ 0.1114\ 0.2935\ 0.1114\ 0.3276]$$

Finally, Eq. (7) is used to obtain the comprehensive prospect value of each MWTC.

$$V_1 = -0.2127,\ V_2 = -0.9166,\ V_3 = 0.3831$$

MWTCs sorted in descending order at infectious risk is represented as follows: $A_3 > A_1 > A_2$. This means that NewB-T is the optimal MWTC, followed by Special-T and Reconstructed-T. For decision-makers, NewB-T is the best solution if only the minimum risk is considered. However, both risk and cost are critical factors in practice, and decision-makers should consider all aspects and then make the final decision.

Eq. (24) is solved using the software package Lingo 18.0, and the multi-objective transportation route optimization result is obtained. The optimal transport route of IMW between three designated hospitals and three MWTCs, when cost and risk are targeted, is obtained. The results indicate that W-one and W-two should transport IMW to Reconstructed-T and W-three should select Special-T.

### 5.4. Discussion

To reflect the effects of $\alpha,\beta$, and $\lambda$ on the risk-avoiding capability of MWTCs in CPT, Table 4 presents the corresponding results based on different $\alpha,\beta$, and $\lambda$ values. From Table 4, we know that parameter values have no influence on the sorting results and have a slight effect on the cumulative prospect values. Therefore, we determine the values of these parameters as $\alpha = 0.88, \lambda = 2.25$, which is feasible both in theory and in practice. Prevention and control measures during an epidemic can affect the transmission probability $\beta$, and the development of new drugs and treatments can increase the cure rate $\omega_0$. To reflect the effects of $\beta$ and $\omega_0$ on waste quantity and confirmed patients, Table 5 presents the corresponding results based on different $\beta$ and $\omega_0$ values.

When $\beta = 2.1101^{-0.8}, \omega_0 = 0.46634$, we can obtain the predicted results as shown by the bolded data in Table 5 and the dynamic evolution curve of diagnosed patients. As shown in Fig. 3, the solid line is the trajectory of predicted values, and the dashed line is the real values of Wuhan city, Hubei Province, China during the epidemic. The two curves basically fit in quantity and trend, which can prove the rationality of selected parameters. If the epidemic changes dynamically, we can adjust the parameters to achieve the purpose of prediction.
6. Conclusions

Due to the specificity, recurrence and universality of COVID-19, this paper correlates waste quantity closely with confirmed cases. Then, based on the relationship, this paper proposes a hybrid two-stage method, which includes a time evolution model for IMW prediction and a multi-objective route optimization model considering risk and cost factors. Several main conclusions are drawn.

First, infectious disease models can be applied to solve many problems, but the model details are heterogeneous by different scenarios and influencing factors. The modified SEIR model considers the isolation measure and asymptomatic infected individuals to modify original approaches, which can further seek the quantitative relationship between waste and confirmed cases to establish the novel forecasting method.

Second, choosing suitable MWTCs and transportation routes may make waste management effectiveness more prominent. The waste route optimization model that takes into consideration infection risk and socioeconomic stress is provided. The model is built and solved based on the predicted values from the previous stage to achieve a dynamic linkage between the two stages.

Third, an illustrative example is given to show the effectiveness of the hybrid two-stage method. Sensitivity analysis is then performed on some of the important parameters, and the predicted values are fitted to the actual values for comparison.

This research has presented evidence that shows that massive infections triggered by the COVID-19 pandemic led to an increase in IMW quantity and to transportation pressures. These problems have been reflected in this paper. The results indicate that infectious medical waste disposal during the pandemic may have been influenced by contagious characteristics, and may cause momentous impacts on transportation routes. Detailed knowledge of waste forecasting and management during emergency events may drastically help to improve management effectiveness. The prediction and management of infectious medical waste widely exist in pandemic challenges around the world. Therefore, there are still many fields for future researches. For example, monetizing the infection risk during the COVID-19 pandemic is an important reference for quantitatively measuring the level of waste risk management. Of course, based on different types of patients with mild, common and severe disease, researchers can also refine the prediction model more precisely.

Data availability

Data will be made available on request.

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References

Alihaf, S., Babbitt, C.W., Chen, R., 2019. Forecasting electronic waste flows for effective circular economy planning. Resour. Conserv. Recycl. 151 https://doi.org/10.1016/j.resconrec.2019.09.038.

Aman, S., Pratama, M.I., Rifandi, M., et al., 2020. Stability analysis and numerical simulation of SEIR model for pandemic COVID-19 spread in Indonesia. Chaos, Solitons Fractals 139. https://doi.org/10.1016/j.chaos.2020.110772.

Aung, T.S., Luan, S.J., Xu, Q.Y., 2019. Application of multi-criteria decision approach for the analysis of medical waste management systems in Myanmar. J. Clean. Prod. 222, 733–745.

Chang, D.Y., 1996. Applications of the extent analysis method on fuzzy AHP. Eur. J. Oper. Res. 95 (3), 649–655.
Yao, L.M., Xu, Z.W., Zeng, Z.Q., 2019. A soft-path solution to risk reduction by modeling medical waste disposal center location allocation optimization. Risk Anal. 40 (9), 1863-1886.

You, S.M., Sonne, C., Ok, Y.S., 2020. COVID-19’s unsustainable waste management. Science 368 (6498), 1438-1439.

Zhao, J., Huang, L.X., Lee, D.H., et al., 2016. Improved approaches to the network design problem in regional hazardous waste management systems. Transport Res E-Log 88, 52-75.

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