Prediction of Compound Bioactivities Using Heat-Diffusion Equation

Graphical Abstract

Highlights

- Prediction model based on heat-diffusion equation (PM-HDE) was constructed

- PM-HDE succeeded in increasing the hit ratio and identifying potent compounds

- PM-HDE discovered new chemotypes in compound evaluation with an ALS-patient iPSC panel

- PM-HDE could represent an algorithm for future drug discovery with AI

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In Brief

Compound screening is a useful tool for discovering new candidate drugs. However, it is still a major challenge, as it is extremely time-consuming and very costly to evaluate millions of compounds. We established a prediction model based on the heat-diffusion equation (PM-HDE) to predict hits in compound screening. PM-HDE succeeded in increasing the hit ratio, identifying compounds with potent broad-spectrum efficacy, and discovering new chemotypes in actual compound evaluation in phenotypic screening.
Prediction of Compound Bioactivities Using Heat-Diffusion Equation

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https://doi.org/10.1016/j.patter.2020.100140

SUMMARY

Machine learning is expected to improve low throughput and high assay cost in cell-based phenotypic screening. However, it is still a challenge to apply machine learning to achieving sufficiently complex phenotypic screening due to imbalanced datasets, non-linear prediction, and unpredictability of new chemotypes. Here, we developed a prediction model based on the heat-diffusion equation (PM-HDE) to address this issue. The algorithm was verified as feasible for virtual compound screening using biotest data of 946 assay systems registered with PubChem. PM-HDE was then applied to actual screening. Based on supervised learning of the data of about 50,000 compounds from biological phenotypic screening with motor neurons derived from ALS-patient-derived induced pluripotent stem cell models (ALS-patient iPSC panel), this algorithm could contribute to the acceleration and development of future drug discoveries using AI.

INTRODUCTION

During the past several years many compounds have been developed for intractable diseases, yet many diseases remain without a treatment. Compound screening, especially phenotypic screening with human induced pluripotent stem cells (iPSCs), is a useful tool for discovering new candidate drugs and disease pathways even if the disease mechanism has not
been completely clarified. Nevertheless it is still a major challenge, as it is extremely time-consuming and very costly to evaluate millions of compounds. Notwithstanding these hurdles, the method for prediction of the effectiveness of compounds is expected to promote cell-based drug discovery. In the hit prediction using an inductive prediction method based on machine learning, such as quantitative structure-activity relationship (QSAR), support vector machine (SVM), random forest (RF), deep learning, and clustering based on structural similarity, compound activity can be predicted from the structure of the unassayed compound by learning the relationship between molecule descriptors and fingerprints derived from the chemical structure of the reference data and the activity value. However, due to the inherent complexity of phenotypic screening, there have been several challenges to predicting activity by conventional methods, including lack of flexibility for dealing with imbalanced datasets, non-linear prediction, and unpredictability of new chemotypes. The datasets from compound screening present an imbalanced ratio of hits/non-hits, the ratio generally being less than a few percent, with non-linear distribution, and this causes difficulty of precise prediction for conventional machine learning from compound screening. Furthermore, the prediction of new chemotypes not identified in the provided datasets is difficult for conventional machine learning, as it is difficult to determine what kind of features in chemotypes are the most important because of the lack of information related to the new chemotype.

To find further improvements regarding this issue, we established a prediction model based on the heat-diffusion equation (PM-HDE), which is a novel approach that uses a heat-diffusion equation to predict hits in compound screening. The heat-diffusion equation, a partial differential equation, describes how heat conduction and material diffusion distribute in three-dimensional space over time, and this can be expanded to a multi-dimensional space for further analysis. It calculates “active” and “inactive” separately by scoring each compound and adjusts spatial integration appropriately, showing a flexibility for accurate prediction. This feature can be expected to work better than alternative conventional methods. Validation of PM-HDE was conducted using 946 PubChem datasets, after which we implemented the algorithm for actual compound screening using iPSC-based phenotypic screening for drug discovery.

**RESULTS**

The heat-diffusion equation, a partial differential equation, describes how heat conduction and material diffusion distribute in three-dimensional space over time. The state of heat diffusion over time was schematically shown from the initial state \( t = 0 \) to the appropriate time points at which the unknown region is filled by heat diffusion (Figure 1A). The heat-diffusion equation puts each reference compound in a small region in the chemical space (hereafter referred to as “mesh”), and they do not overlap with each other. Thereby, the impact of heat diffusion from each mesh to the whole space is clearly defined and their sum remains constant during the diffusion process. In addition, because the heat-diffusion equation calculates heat-diffusion processes of positive heat values from active compounds and negative heat values from inactive ones independently and do not interfere with each other, the ratio of the total quantity of positive heat values and that of negative heat values is always unchanged. Therefore, by adjusting the coefficient \( C \) as a reciprocal of the ratio, the total quantity of both positive and negative heat is always zero even in the case of an imbalanced active ratio. As a result, each point in the space can be predicted as active compound or inactive compound based on the plus and minus of the prediction score, described as Virtual Score (V-Score) (Figure 1B). The details of the mathematical methods are described in Experimental Procedures. In addition, since PM-HDE itself is a non-linear prediction model, it is possible to flexibly cope with complex relationships between descriptors and activity. Furthermore, by adjusting the diffusion time \( t \), it is possible to predict a compound which is at a position away from the reference mesh group in the chemical space, that is, a compound that is not similar to the active compound contained in the reference data. Using these features, we applied the heat-diffusion equation to build a prediction model for phenotypic screening, PM-HDE, which can predict the hit compounds by formulating heat diffusion and applying molecular descriptors derived from the chemical structure into this formula to calculate the prediction score shown as V-Score. The V-Score is calculated as the temperature of heat diffusion, and compounds could be ranked based on the predicted score (Figure 1C).

**Validation of PM-HDE Using Multiple Bioassay Datasets**

First, 281 molecular descriptors were extracted from a total of 1,273 molecular descriptors to avoid imbalance of specific descriptors and delete invalid descriptor groups (Figure 2A and Table S1). To confirm the feasibility of PM-HDE, we constructed a prediction model for various assay data obtained from PubChem and performed cross-validation to confirm that PM-HDE can solve the issues of the conventional methods. Biotest data of 946 assay systems registered with PubChem were used to validate the predictive performance of PM-HDE in compound screening. The maximum area under the curve (AUC) of 946 assay systems was determined according to the procedure for parameter setting for PM-HDE (Figure 2B). To evaluate the prediction performance, we performed cross-validations on many datasets and calculated each AUC of the receiver-operating characteristics (ROC) curves (Table S2). The relationship between the proportion of active labels and AUC is shown in Figure 2C, suggesting that PM-HDE presented high prediction performance, showing high AUC levels even in datasets with a bias of the active ratio. Even large-sized data could be predicted with high accuracy (Figure 2D). The 946 assay systems we analyzed were mostly via high-throughput screening. However, these were very diverse in that they used enzymes, cells, and nucleic acids as targets, detection methods such as fluorescence, luminescence, and binding assays, focused on inhibition and promotion or agonist/antagonist in terms of the pharmacological actions, and were performed for the purpose of drug development and ADMET evaluation. We classified the prediction performance according to assay types and found that similar high-precision predictions could be obtained with both phenotypic assay and target-based assay (Figure 3A), demonstrating that the issues of conventional methods for datasets showing complex activity data such as a phenotypic assay can be solved by using PM-HDE.
To investigate the relevance between V-Score and activity, the PubChem Score, and the structural similarity with the active label compound in the training set, hereafter referred to as the parent compound, were plotted for each system. It was clear that the compounds that included top-ranked compounds, within 0.0%–0.5% fraction, tended to have a much higher PubChem Score (Figure 3B). On the other hand, no apparent difference was observed in the structural similarity with the parent compound (Figure 3C). This means that the compounds ranking highest in the test set are not necessarily those with high structural similarity to the parent compound. That is, the V-Score may be expected to be high, depending on the molecular descriptors, even if structural similarity with the parent compound is not so high, and as a result PM-HDE has the potential to discover new chemotypes. This indicates that the V-Score in this method well reflects the value of the actual PubChem Score.

Performance of PM-HDE was compared with the k-nearest neighbor (kNN), RF, and SVM, as the well-known in silico predictors (Table 1). PM-HDE has a potential to show higher accuracy than kNN, especially in datasets with large entity and low active ratio. PM-HDE also presented competitive or superior accuracy compared with RF and SVM.

Implementation of PM-HDE in Compound Screening Using Human Motor Neurons

To make this model practical, we applied PM-HDE to perform hit prediction of iPSC-based phenotypic screening for amyotrophic lateral sclerosis (ALS). ALS is a lethal neurological disease in which motor neuron death causes muscle weakness and atrophy.11,12 Since there have been no radical treatments, the development of a medicine for ALS is an urgent medical need. Motor neurons were derived from sporadic ALS-patient iPSCs (Figure S1; Table S3), and a phenotypic screening system to evaluate compounds that inhibit motor neuron death was constructed as previously reported.13 This system produces motor neurons from iPSCs in 7 days, followed by motor neuron death in the next 7 days. After culturing motor neurons in 384-well plates with compounds for 7 days, the number of surviving motor neurons was automatically measured by high content analysis (Figure 4A). Figures of motor neurons on day 6 and day 14, which were treated with inactive compound or active compound from day 6 to day 14, are shown in Figure 4B. The stability and quality of the screening system were proved by the evidence of a low coefficient of variation (Figure 4C) and a high Z\textsuperscript{0} factor (Figure 4D). The hit criterion was defined as a compound that inhibited 60% or more of motor neuron death. Using this screening system, 48,415 compounds...
selected from the corporate library were used for first screening, and 174 hits were obtained (Figure 4E). The hit ratio was 0.36%.

Although phenotypic screening has the advantage of finding an active compound that directly reflects the disease phenotypes, evaluation of millions of compounds presents a major hurdle in terms of time and cost. Therefore, we applied PM-HDE to predict active compounds (Figure 5A) following determination of the best parameter sets (Figures 5B and 5C). Simulation of >1.6 million compounds was conducted based on first screening data, and 5,875 compounds were prioritized for evaluation of their suppressive effects against motor neuron death based on the V-Scores. The predicted active compounds were evaluated using ALS motor neurons by in vitro experiments. Details of the screening procedure are described in Figure 5D. In total, 5,875 compounds were added to ALS motor neurons derived from patient iPSCs to evaluate their effects on motor neuron death, and 252 hits were obtained (Figure 5E). The hit rate was 4.3%, a 10-fold increase compared with the first screening. Furthermore, when the structures of the 252 hits were examined, 16.7% of the compounds presented a new chemotype showing 50% or less similarity with any parent compounds (Figure 6A). These results suggested that PM-HDE could be useful for increasing hit efficiency and finding new chemotypes.

Next, we selected compounds without effects of cell proliferation, antioxidant, or kinase inhibition for further evaluation from the compounds presenting mainly 50% or less similarity with any parent compounds. The PM-HDE strategy successfully discovered five new chemical series that had not been identified by other screening approaches, showing little similarity between respective compounds as well as with riluzole and edaravone, which have been approved by the Food and Drug Administration for the treatment of ALS (Figure 6B).

Verification of Output of PM-HDE Using Biological Assays

Finally, the compounds identified by PM-HDE followed by the further selection described above were verified using ALS iPSC panels consisting of motor neurons derived from multiple ALS-patient iPSCs. Since sporadic ALS is known to harbor genetic heterogeneity, evaluation of drug responsiveness using iPSCs from multiple ALS patients is required. To evaluate the robustness of compound efficacy, we conducted ALS iPSC panel trials composed of motor neurons from 29 iPSC clones derived from multiple sporadic ALS patients as previously reported (Figures 7A and S1), and the efficacy of five compounds identified by PM-HDE was evaluated (Figure 7B). In addition, the efficacy of each compound was compared with riluzole and edaravone (Figure 7C). The compounds identified by PM-HDE demonstrated broad and potent effectiveness against motor neuron death in clones derived from various sporadic ALS patients.
DISCUSSION

PM-HDE was used in million-scale compound screening to identify promising lead compounds and new chemotypes. The robustness of PM-HDE was verified using PubChem data and was then applied to ALS iPSC-based phenotypic screening, resulting in the identification of potent compounds with a broad spectrum covering multiple iPSC lines from ALS patients. With regard to the heat-diffusion equation, it is a differential equation that requires integration constants in order to have a unique solution describing the distribution of heat in a particular body over time. The equation has other important applications in mathematics, statistical mechanics, probability theory, and financial mathematics. PM-HDE is the first application of the heat-diffusion equation to drug discovery.

In past years, although molecular target-based drug screening has been the main drug discovery paradigm, there appears to be recent renewed interest in phenotypic screens for drug discovery. Phenotypic screening by pathologically relevant cellular models using patient-derived iPSCs has the potential to find new candidate drugs and disease pathways even for the disease whose etiology has not yet been completely clarified, and it is possible to discover the potential efficacy of compounds beyond the limitations of target-based screening.

In the heat-diffusion equation, the ratio of active compounds to inactive compounds is defined as a volume ratio to the entire space by considering the mesh (described as C in Experimental Procedures). In PM-HDE, the reference data are calculated by mapping them to a mesh in chemical space. Since meshes have a definite size, we can give each one a heat value and define its ratio to the total chemical space. In this case, C adjusts the sum of the heat value of the active and inactive data groups so that the total heat value is always zero at any diffusion time. Wherever the test data are located in the chemical space, the sign of the prediction score (V-Score) can be used to determine whether the data are in the active or inactive region at diffusion time t. If one does not adjust for C, any region in the chemical space may be marked as active, depending on the ratio of actives in the reference data. Thus, PM-HDE can be used for imbalanced datasets since it can set the sum of the entire space to zero by taking the inverse of C. Thus, PM-HDE provides flexibility by adjusting h, even if it is a separation problem or a quantitative prediction that reflects the intensity of compound activity.

In phenotypic assays, as the factors affecting activity are diverse and complex, the relationship between molecular descriptors and activity also becomes complex and is not linear. Therefore, in QSAR and SVM, which are prediction models of linear regression, it is necessary to make an adjustment so as to enable linear separation using a kernel function, but there is a risk of overfitting by this adjustment, and there is a concern that extrapolation may be reduced. Furthermore, while prediction based on structural similarity can find active compounds with a high probability, it is challenging to find new chemotypes because only compounds similar to the parent compounds in the reference data can be selected. PM-HDE can be expected to maintain prediction performance even with datasets with large bias in the ratio of active compounds in the reference data. In addition, since PM-HDE itself is a non-linear equation, it is possible to flexibly cope with complex relationships between descriptors and activity. By adjusting the diffusion time t, it is possible to predict a compound which is at a position away from the reference mesh group in the chemical space, that is, a compound that is not similar to the active compound contained in the reference data. Furthermore, the PM-HDE algorithm is suitable for parallelization, and it can learn at high speed even when dealing with myriad reference data and many descriptors.
It is easy to interpret the influence of each piece of activity information contained in reference data and each descriptor used for training for the prediction result.

In this study, although we have compared PM-HDE with other machine-learning methods using several benchmark datasets, the number of comparisons was limited and the only performance comparison in actual screening was against random screening. Further verifications are desired for the widespread application of PM-HDE. Recently, conventional machine learning has evolved into new methods to improve the performance. Furthermore, deep-learning methods have also been developed and applied to drug discovery with flexibility. These methods are expected to contribute to drug development, and the choice of each method may depend on experimental uncertainty regarding the data and dataset size.

Table 1. Comparison of PM-HDE with In Silico Hit Predictors

| AID       | Assay Description                                                                 | Entries in Dataset | Actives | Active Ratio | PM-HDE AUC | kNN AUC | RF AUC | SVM AUC |
|-----------|-----------------------------------------------------------------------------------|--------------------|---------|--------------|-------------|---------|--------|---------|
| 0000097   | NCI human tumor cell line growth inhibition assay. Data for the HS 578T breast cell line | 25,421             | 1,378   | 5.42%        | 0.86        | 0.85    | 0.77   | 0.85    |
| 0000361   | Pyruvate kinase                                                                   | 50,585             | 602     | 1.19%        | 0.86        | 0.85    | 0.83   | 0.86    |
| 0000881   | qHTS assay for inhibitors of 15-hLO-2 (15-human lipoxigenase 2)                  | 104,068            | 574     | 0.55%        | 0.91        | 0.86    | 0.86   | 0.90    |
| 0000885   | qHTS assay for activators of cytochrome P450 3A4                                | 12,561             | 159     | 1.27%        | 0.92        | 0.92    | 0.89   | 0.93    |
| 0001457   | qHTS assay for identifying the cell-membrane permeable IMPase inhibitors: potentiating with lithium | 202,356            | 722     | 0.36%        | 0.83        | 0.79    | 0.8    | 0.82    |
| 0002842   | High-throughput screen of a putative kinase compound library to identify inhibitors of Mycobacterium tuberculosis H37Rv | 23,462             | 1,248   | 5.32%        | 0.91        | 0.91    | 0.85   | 0.89    |
| 0624173   | qHTS of Trypanosoma brucei inhibitors                                            | 400,566            | 483     | 0.12%        | 0.91        | 0.87    | 0.91   | 0.91    |
| 1159515   | qHTS assay to identify small-molecule agonists of the nuclear factor κB signaling pathway-cell viability counter screen | 6,228              | 190     | 3.05%        | 0.84        | 0.84    | 0.85   | 0.84    |

qHTS, quantitative high-throughput screening.

Figure 4. iPSC-Based Phenotypic Screening and Constructing Datasets for PM-HDE
(A) Screening system for the evaluation of ALS motor neuron survival.
(B) ALS motor neurons derived from patient iPSCs. Cells were stained with TUBB3, a marker for neurons.
(C) Flat test of the screening.
(D) Z’ factor of the screening.
(E) Activity distribution of 48,415 compounds in the first screening. The hit criterion was defined as a compound that inhibited 60% or more of motor neuron death (shown as red line), and 174 hits were obtained.
PM-HDE could be a powerful tool to discover promising lead compounds for drug development. It may be possible to screen unlimited numbers of compounds, and widening its application to drug discovery for various other diseases is also expected.

EXPERIMENTAL PROCEDURES

Resource Availability

Lead Contact

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Materials Availability

The study did not generate new unique reagents.

Data and Code Availability

The BioActivity data, descriptors, and SD-file can be downloaded from PubChem’s FTP site (BioActivity data: ftp://ftp.ncbi.nlm.nih.gov/pubchem/Bioassay/Concise/CSV/Data); descriptions: ftp://ftp.ncbi.nlm.nih.gov/pubchem/Bioassay/Concise/CSV/Description); SD-files: ftp://ftp.ncbi.nlm.nih.gov/pubchem/Compound/CURRENT-Full/SDF). The code supporting the current study have not been deposited in a public repository because the authors are currently in the process of patenting the code, but are available from the Lead Contact on request.

Mathematical Methods for Heat-Diffusion Equation

The heat-diffusion equation was derived by the following mathematical theory.

\[
(1) \text{ Given data} \\
\text{Reference data are calculated separately for the active and inactive groups.} \ z \ (\text{the value of criterion}), \ \text{[active reference data]} \ \hat{P}^{a} (k) \cdot \text{descriptor (n-dim.) vector}, \ z^{a} : \text{score of the kth data (e.g., value of biological activity)}; \ z^{a} \text{for } k = 1, \ldots, m_{1}, \ \text{[inactive reference data]} \ \tilde{P} (k) \cdot \text{descriptor (n-dim.) vector};
\]
Assign data with the same descriptor vectors.

Fix mesh size 0. Set cube $Q_j = \prod_{i=1}^{n} [a_i - 1, a_i + 1]$, for $j = (j_1, \ldots, j_n)$.

Normalization is performed for each descriptor, then binned and allocated to one of the ranges. By allowing all descriptors to do this, one reference datum is assigned to a mesh somewhere in the chemical space.

**Method B:** Both active and inactive compounds should be excluded from the reference data set. If $Q_j$ contains at most one reference datum, then $Q_j$ is denoted by $J^*(k) = \{j_1(k), \ldots, j_n(k)\}$ (resp. $J^*(k) = \{j_1(k), \ldots, j_n(k)\}$).

When compounds are assigned to a mesh, a mesh with a composition of both active and inactive compounds should be excluded from the reference data. If a mesh is assigned to multiple active or inactive members, the activity value of the mesh is represented by the average of the members.

**Heat-diffusion equation**

The contribution from one reference datum to the test data is calculated for each mesh using the following formula:

$$u^+(\bar{x}, t; k) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} \frac{e^{-z^2}}{C_0} \, dz$$

for Method A.

$$u^+(\bar{x}, t; k) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} \frac{e^{-z^2}}{C_0(\bar{x}, k)} \, dz$$

with $b^+_i(k) = (j^+_i(k) - 1/2)\eta$ for Method B.

In actuality, the coefficient of $1/(4\pi t)^{n/2}$ does not need to be calculated.
Figure 7. ALS iPSC Panel Trials for Compound Evaluation
(A) Representative figures of motor neurons listed in an ALS iPSC panel consisting of motor neurons derived from 29 clones from sporadic ALS patients. Motor neurons in the ALS iPSC panel recapitulated ALS motor neuron death.
(B) Evaluation of the active compounds extracted from PM-HDE using the ALS iPSC panel. 1 μM, 3 μM, and 10 μM concentrations of five compounds were evaluated using 29 ALS clones (n = 3 in each clone). Effects of riluzole and edaravone were also evaluated.
(C) Efficacy of the compounds was compared with those of riluzole and edaravone showing potent efficacy on ALS motor neuron rescue (n = 29 clones, one-way ANOVA; *p < 0.05).
where \( u^A(x, k) = \begin{cases} 1, & x \in Q_{A \cap k}^- \\ 0, & \text{otherwise} \end{cases} \) for Method A, \( u^B(x, k) = \sum_{i=1}^{|z|} \delta(i(x-b^i(k))) \) for Method B, and \( \delta \) is Dirac’s \( \delta \)-function (decoding the same order).

Using the equation in (3), we integrate (4) for all meshes to obtain a predicted score for the test data. For each reference data value, the difference between the activity value \( (v_k) \) and the criteria \( z \) is taken, the difference is multiplied by seven different \( h \) in hyperbolic tangent \( \tanh \), and the weight is given according to the activity value. In other words, we can reflect the intensity of the activity as the heat value, because the weight of the activity differs between ones that greatly exceed the criteria and ones that are close to the criteria. In addition, by using \( \tanh \), the correspondence between the activity value and the weighting can vary smoothly from near-linear to logarithmic to determine the appropriate weighting parameter 0

\[ i^\pm(u; x) = \frac{1}{2} (i^+(u; x) - i^-(u; x)) \]

\[ 1. \text{ Contribution from each mesh:} \]

\[ u^+ (x, k, t) = \prod_{i=1}^{|z|} \delta^+(i(x-b^i(k))) \]

\[ n = 281 \text{ (data dimension)} \]

\[ 2. \text{ V-Score for an unknown compound:} \]

\[ f(x, t, h) = \sum_{i=1}^{|z|} u^+(x, t, k) \tanh(h(v_z - z)) - C \sum_{i=1}^{|z|} u^-(x, t, k) \tanh(h(z - v_z)), \]

\[ C = \sum_{i=1}^{|z|} \tanh(h(v_z - z)) / \sum_{i=1}^{|z|} \tanh(h(z - v_z)), \]

where \( x \) : description vector of unknown compound, \( t \) : diffusion time, \( k \) : reference data ID, \( b^i(k) \) : the \( i \)th descriptor’s value of the center point of the mesh in which the \( k \)th reference data \( (+, \text{active}; -, \text{inactive}) \) are contained, \( v_z \) : activity score of the \( k \)th reference data, \( z \) : criterion of the assay, \( m1 \) : number of active meshes, \( m2 \) : number of inactive meshes, \( h \) : weighting parameter 0.005, 0.01, 0.02, 0.05, 0.1, 0.2, \( \infty \).

In the prediction, the parameter set \( t, h \) should be determined beforehand for maximum AUC based on cross-validation. Multiple reference compounds with the same label in a mesh are also calculated as a single reference compound. On the other hand, if reference compounds with different labels correspond to a mesh, the mesh will be considered as noise data and will be considered invalid and not used in model generation. By including this kind of preprocessing, the noise in the reference compound can be greatly reduced.

### Acquisition of Biological Activity Data and Chemical Structures from Public Data

The Bioactivity Data (concise version), descriptions, and SD-file were collectively downloaded from PubChem’s FTP site on May 30, 2016. Based on these files, we first created a biological activity data file for each Assay ID (AID) and an assay name list. In the biological activity data file, only those records in which \( \text{ACTIVITY \_OUTCOME} \) was labeled active or inactive were included. Furthermore, conditions for selecting a system to be analyzed were defined as the number of compounds of 8,000 or more, excluding duplications based on Compound ID (CID), the number of active labels of 10 or more, the \( \text{ACTIVITY \_SCORE} \) range of 2 or more, after which CID, \( \text{ACTIVITY \_OUTCOME} \), and \( \text{ACTIVITY \_SCORE} \) (hereafter abbreviated as “PubChem Score”) were output.

The criterion of each assay system was defined as the midpoint of the \( \text{ACTIVITY \_SCORE} \) boundary values of the Active label and the Inactive label. Biological activity data files were prepared for the 946 assay systems selected above. A part of the list is shown in Table S1.

Next, structure information described in the Connection Table corresponding to all the CIDs was extracted from the SD-files and desalted into a single molecule; then those containing isotopes, fraudulent valence, inappropriate atomic species, radicals, and super macromolecules were excluded. To eliminate mistakes of structural formulas, only those records in which the Connect Table in the SD-file and isomeric SMILES contained in the Data field including stereoscopic information were consistent were considered as valid structural data.

### Generation and Selection of Molecular Descriptors

The SD-file was converted into isomeric SMILES using mol2smi ver.4.95 (Daylight Chemical Information Systems, Aliso Viejo, CA), then the most stable 3D-conformer was generated using Omega ver.2.5.1.4 (OpenEye Scientific, Santa Fe, NM). Using the SD-file with a three-dimensional coordinate as input, we calculated all 1,273 molecular descriptors that can be generated using CORINA Symphony Descriptor Ver.1.0 (Molecular Networks, Nürnberg, Germany). Because the original 1,273 molecular descriptors contain many vectorial data, analyzing all of them is not practical due to the overfitting of specific descriptors. Therefore, the proportions of records with invalid values, correlation coefficient, skewness, and kurtosis were calculated for all molecular descriptors, and 281 descriptors considered necessary and sufficient for the subsequent analyses were selected (Table S2). These 281 descriptors were fixed throughout this study. We merged these data with the biological activity data using CID as a key and created an input file for analysis for each assay system.

### Normalization and Data Cleansing

Irrelevant data contained in the input files were cleansed by following these procedures.

1. Mean and standard deviation were determined for each of the 281 molecular descriptors and normalized for all values.
2. The values of (1) were binned every 0.1 and assigned to 281-dimensional mesh space using them as grid points.
3. When multiple data corresponded to the same mesh, all data in the mesh were invalidated and excluded from the analysis if there were pairs with different labels as Active/Inactive.

These normalization/cleansing processes were also applied to the preparation of the training set in cross-validation, as described later.

### Coding and Cross-Validation of the Heat-Diffusion Equation Program

Coding was performed using the 64-bit version of Visual C++ 2013 (Microsoft, Redmond, DC) according to the algorithms shown in Figure 1B. The prediction score for one record in a test set is referred to as the V-Score in Table S1. It is expressed by \( f(x, t) \), and corresponds to the temperature in the original definition.

After cleansing the data groups of each assay system, we divided the data into a training set (test set \( = 9:1 \)) and performed cross-validation. For each test set, by giving the diffusion time \( t \) as 6.0 to 12.0, the AUC of the ROC curve was calculated for each of the 31 \( \times 7 = 217 \) patterns of parameters as calculation parameters, and the mean and standard deviation of 217 values for the test sets were calculated to determine the best-suited parameters. These series of calculations were performed in a batchwise manner for 946 assay systems.

### Analysis of the Relationship between V-Score and Structural Similarity

The means of active label capture rate, PubChem Score, and structural similarity between training set and test set were examined for the 0.0%–0.5% fraction and the 5.0%–5.5% fraction from the top of the V-Score in each of the 713 systems that gave a local maximum of AUC and showed a standard deviation...
of ≤0.12 with a maximum AUC of ≥0.65 among the 946 assay systems. Structural similarity was obtained by calculation of the Tanimoto coefficient following the generation of 2,048 bit fingerprints using Daylight’s Toolkit ver. 4.95 based on isomeric SMILES.

**The k-Nearest Neighbor, Support Vector Machine, and Random Forest**

The Python library “scikit-learn” was employed for the development of kNN (sklearn.neighbors.KNeighborsClassifier), SVM (sklearn.svm.SVC), and RF (sklearn.ensemble.RandomForestClassifier) classification models. All methods employed used 10-fold cross-validation to identify their hyper-parameters, i.e., the number of neighbors to use k for kNN, penalty parameter C, and nuclear parameter γ for SVM, and maximum depth, the minimum number of samples required to split an internal node, and the minimum number of samples required to be at a leaf node for RF. A 10-fold cross-validation was implemented by first dividing the training set into ten equal groups, nine of which were used for model construction and the tenth for validation. Series of hyper-parameter values were respectively assigned to construct the models, and by determining the best AUC values the optimal ones were identified.

**Generation of iPSCs**

iPSCs were generated from skin fibroblasts or peripheral blood mononuclear cells of sporadic ALS patients using episomal vectors ( Sox2, Klf4, Oct3/4, L-Myc, Lin28, and p53-short hairpin RNA) as reported previously. Established iPSCs were cultured on an SNL feeder layer with human iPSC medium (primate embryonic stem cell medium; ReproCELL, Yokohama, Japan) supplemented with 4 ng/mL basic fibroblast growth factor (Wako Chemicals, Osaka, Japan) and penicillin/streptomycin or cultured under feeder-free conditions on laminin-511-E8 (Nippi, Tokyo, Japan)-coated plates with StemFit AK01 (Ajinomoto, Tokyo, Japan). The information on iPSC clones is listed in Table S3. Karyotyping was performed by Nihon Gene Research Laboratories (Sendai, Japan).

**Generation of Motor Neurons and ALS iPSC-Based Phenotypic Screening**

Motor neurons were generated from iPSCs as previously described. A poly-cistronic vector containing mouse Lhx3, mouse Mgn2, and mouse Islet1 under control of the tetracycline operator, which was generated from KW110_PB_TA_ERN (Ef1α_rtTA_neo) vector backbone with rtTA and neomycin resistance gene, was co-transfected along with a pHIL-EF1α-hCP-Bace-A encoding transposase into iPSCs using lipofectamine LTX (Thermo Fisher Scientific, Waltham, MA). After clone selection using neomycin, iPSCs carrying the tetracycline-inducible motor neuron differentiation cassette were established.

These iPSCs were dissociated to single cells using Accutase (Innovative Cell Technologies, San Diego, CA) and plated onto Matrigel-coated 384-well plates (PerkinElmer, Waltham, MA) with Neuronal Medium DMEM/F12 (Thermo Fisher Scientific), N2 (Thermo Fisher Scientific) containing 1 μM retinoic acid (Sigma), 1 μM Smoothened agonist, 10 ng/mL brain-derived neurotrophic factor (R&D Systems, Minneapolis, MN), 10 ng/mL glial-cell-line-derived neurotrophic factor (R&D Systems), and 10 ng/mL NT-3 (R&D Systems) with 1 μg/mL doxycycline (TaKaRa, Kusatsu, Japan), and cultured for 7 days. The compounds were added on day 6 or day 7, and cells were fixed in 4% paraformaldehyde and stained with anti-βIII-tubulin (TUBB3) antibody conjugated with Alexa 488 (Sigma) on day 14. Images of motor neurons were acquired by Opera Phenix (PerkinElmer) followed by quantification of the number of surviving motor neurons stained with neuronal marker TUBB3 using the analysis software Harmony (PerkinElmer). The effect of compounds was described as “motor neuron rescue.” Motor neuron rescue (%) = (IX – CJ)/CT × 100, where X: number of motor neurons treated with compounds on day 14, C: number of motor neurons treated with dimethyl sulfoxide group on day 14, T: Number of motor neurons in pretreatment on day 6 or day 7.

**Statistical Analysis**

Results were analyzed using one-way ANOVA followed by Dunnnett’s post hoc test to determine statistical significance of the data. Differences were consid-
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