Differentiating *Plasmodium falciparum* alleles by transforming Cartesian X,Y data to polar coordinates

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Abstract

**Background:** Diagnosis of infectious diseases now benefits from advancing technology to perform multiplex analysis of a growing number of variables. These advances enable simultaneous surveillance of markers characterizing species and strain complexity, mutations associated with drug susceptibility, and antigen-based polymorphisms in relation to evaluation of vaccine effectiveness. We have recently developed assays detecting single nucleotide polymorphisms (SNPs) in the *P. falciparum* genome that take advantage of post-PCR ligation detection reaction and fluorescent microsphere labeling strategies. Data from these assays produce a spectrum of outcomes showing that infections result from single to multiple strains. Traditional methods for distinguishing true positive signal from background can cause false positive diagnoses leading to incorrect interpretation of outcomes associated with disease treatment.

**Results:** Following analysis of *Plasmodium falciparum* dihydrofolate reductase SNPs associated with resistance to a commonly used antimalarial drug, Fansidar (Sulfadoxine/pyrimethamine), and presumably neutral SNPs for parasite strain differentiation, we first evaluated our data after setting a background signal based on the mean plus three standard deviations for known negative control samples. Our analysis of single allelic controls suggested that background for the absent allele increased as the concentration of the target allele increased. To address this problem, we introduced a simple change of variables from customary (X,Y) (Cartesian) coordinates to planar polar coordinates (X = rcos(θ), Y = rsin(θ)). Classification of multidimensional fluorescence signals based on histograms of angular and radial data distributions proved more effective than classification based on Cartesian thresholds. Comparison with known diallelic dilution controls suggests that histogram-based classification is effective for major:minor allele concentration ratios as high as 10:1.

**Conclusion:** We have observed that the diallelic SNP data resulting from analysis of *P. falciparum* mutations is more accurately diagnosed when a simple polar transform of the (X,Y) data into (r,θ) is used. The development of high through-put methods for genotyping *P. falciparum* SNPs and the refinement of analytical approaches for evaluating these molecular diagnostic results significantly advance the evaluation of parasite population diversity and antimalarial drug resistance.

**Background**

Evaluating genotype data of pathogens isolated from a single human host presents an important challenge for molecular diagnostic assays as each human sample can contain varying numbers of parasite strains [1]. Genotype data for many diagnostic technologies are reported across a scale of fluorescence, though further evaluation is necessary to understand how fluorescence units correspond to the number of infecting pathogens. Further complications are encountered if the pathogen is diploid, if target sequences of interest are repeated in single-copy genomes, or if haplotype resolution is a necessary component of diagnosis [2].

We have recently developed a post-PCR, ligation detection reaction - fluorescent microsphere assay (LDR-FMA) to evaluate single nucleotide polymorphisms...
(SNPs) associated with drug resistance in the notorious malaria parasite, *Plasmodium falciparum* (Pf) [3]. This assay employs Luminex xMAP technology to differentiate between possible alleles at a given locus. The genotypic fluorescence data generated provides semi-quantitative information regarding the relative abundance of haploid parasite strains contained within an individual human patient. In our earlier study, we observed that as the fluorescence signal for single allele positive controls increased with increasing DNA template concentration, fluorescence associated with the allele not present in the sample would increase above background [3].

We approach the problem of accurate genotype identification by transforming bivariate fluorescence data from standard Cartesian (x,y) coordinates into polar (r,θ) coordinates as described below. In the standard Cartesian representation, the x-axis represents the fluorescence signal in an individual sample associated with allele X (typically the wild-type or drug sensitive allele) and the y-axis represents the fluorescence signal associated with allele Y (typically the mutant or drug resistant allele). This polar transformation takes into account the apparently linear crosstalk interaction responsible for the background signal. A similar kind of bivariate transformation has been applied to genotyping of diploid systems [4-7]. In the diploid case, these methods effectively distinguish between small, discrete numbers of possible diploid copy numbers (e.g. 0, 1 or 2 allelic copies). Our method distinguishes infection by either, both, or neither form of an allele that may be present in any given sample in an effectively continuous range of possible copy numbers.

Accurate classification of background and positive signal is essential in evaluation of infection by any pathogenic species and its various strains. In the context of malaria, isolate differentiation is utilized for studies of parasite population diversity and structure, as well as in identification of drug resistant parasites. Precise estimation of parasite population diversity is essential as this diversity can affect the ability to monitor antimalarial drug efficacy in a region [8]. Genotyping of specific drug resistance loci carries special importance because improper treatment of *P. falciparum* can lead to death of infected patients. Moreover, better identification of drug resistant parasites in endemic populations could be used to revise treatment protocols recommended by Ministries of Health [9] as increasing prevalence of drug resistant parasites has been associated with increased malaria morbidity and mortality [10]. As the arsenal of antimalarial drugs is limited, improved monitoring of drug efficacy and diagnosis of mutations associated with drug resistance is important for programs attempting to control the prevalence of infection by *Plasmodium* species parasites and reduce the potential for mosquito-borne transmission.

**Results and Discussion**

**Motivation for the polar coordinate transformation**

When diallelic SNPs occur in a population of haploid *P. falciparum* blood-stage parasites, infected individuals may be positive or negative for infection by parasites carrying either allele. With respect to any single SNP locus there are four possible infection 'states': X+/Y- (infected by wild-type parasites only), X-/Y+ (infected by mutant parasites only), X+/Y+ (infected by both wild-type and mutant parasites), or X-/Y- (no infection). Three of these states (X+/Y-, X-/Y+, X+/Y+) cannot be distinguished using standard blood smear microscopy because the SNP does not confer observable changes in parasite morphology. The goals of the present study were to distinguish the infection states of individuals in an endemic population and to establish levels of confidence in the diagnostic assessment.

Unlike genotyping results on single-copy loci from diploid organisms, where allele-specific signals are based on discrete template quantities (0, 1 or 2 allelic copies), allele-specific signals for *P. falciparum* cover a continuous and varying range as a human infection can consist of multiple parasite strains with wide ranging parasitemia levels for each strain. The LDR-FMA procedure produces fluorescence measurements associated with the presence of varying levels of one or two site-specific alleles in a blood sample. Some low-level background signal is observed in control samples containing no DNA. The standard method for establishing the presence of a given allele in a sample is to impose a threshold based on the background signals obtained from a number of blank controls; background signals for alleles of the Pf dihydrofolate reductase gene (*dhfr*) when evaluated in uninfected North American controls ranged from 154 to 322 Median Fluorescence Intensity (MFI) units [3]. A typical threshold would then be set at a fluorescence level of at least two standard deviations above the mean obtained from this ensemble of DNA-negative blanks. In LDR-FMA diagnosis interpretation of true positive from negative fluorescence measurements becomes complicated by background fluorescence signal when, for example, allele "Y" is not present, while allele "X" is present at high levels. Results in Figure 1 illustrate this outcome in a control experiment where LDR-FMA was performed on the *dhfr* SNP occurring at amino acid 164 (sensitive allele = isoleucine [I; codon ATA]; resistant allele = leucine [L; codon TTA]). PCR amplification was performed on a dilution series of the Pf laboratory-adapted strain, 3D7 (*dhfr* 164I). The average background signal when no 3D7 genomic DNA was added to the initial PCR was 95.5 MFI units (3xSD = 156.6 MFI units). At higher concentrations of 3D7 genomic DNA the *dhfr* 164L signal was consistently above the conventional background value (> 200 MFI units).
Because the two sequences differ at only a single base pair, it was not surprising that a small fraction of LDR products representing the 164L allele (not present in 3D7) formed despite sequence mismatch when the concentration of the 164I template increased through PCR amplification. This is particularly true since the mismatched base pairs occur at the end of the oligonucleotide probe sequences and not in middle positions found to be more destabilizing to probe hybridization [11]. In our analyses of field samples from malaria-endemic regions of Papua New Guinea (PNG), we have observed these same background trends in our results. Figure 2 shows an example of bivariate fluorescence data obtained from the LDR-FMA analysis of 264 PNG patients at the dhfr 59 (C/R) locus. This locus was chosen as both alleles are found in the PNG parasite population, in contrast to the dhfr 164 locus. Using the threshold determined as three standard deviations above the mean calculated from known negative samples, these results suggest that 68 individuals (25.8%) were infected with mixtures of 59 C and R (Figure 2). When the XY-plot of this data is examined by eye, there is an obvious increase in background levels for both alleles as the median fluorescence increases (Figure 2). Given that similar results were seen in our dilution control experiment (Figure 1), we were concerned that the conventional approach for differentiating positive from background fluorescence was resulting in over-reporting the number of mixed strain infections. Motivated by the possibility that the background signal could be roughly linearly proportional to the concentration of the non-matching sequence, we introduced a transformation of the (x,y) fluorescence data that is compatible with this natural multiplicative structure in the distribution of the data. We introduce polar coordinates (r,θ) such that

\[ r = \sqrt{x^2 + y^2} \]  
\[ \theta = \arctan \left( \frac{y}{x} \right) \]  

(Figure 3). The magnitude r represents the distance in the plane from the point at (0,0) to the point at (x,y), and provides a measure of the overall level of infection. The quantity θ represents the angle between the x-axis and ray extending from the point at (0,0) to the point at (x,y). The angle θ depends only on the ratio y/x of the two fluorescence signals. If the background signal were truly linear, samples with single strain infections would appear in the Cartesian plane along lines with y/x ratios equal to a constant. Consequently we sought to determine diagnosis thresholds in terms of the angle θ (or equivalently, in terms of the ratio y/x) rather than in terms of x or y alone.

### Histogram based threshold estimation

The four possible states of infection observed through the combination of two allele-specific fluorescence signals occupy four regions of the (X,Y) plane. Results for individuals with monoallelic infections lie near either the x-
or \(y\)-axis, whereas results for mixed strain infections lie somewhere in the upper right region of the plane. Uninfected individuals cluster together near the origin. The classification problem amounts to drawing boundaries somewhere in the upper right region of the plane. Uninfected individuals lie scattered around a vertical line at an angle close to but less than \(\frac{\pi}{4}\) (or 90°). Individuals with mixed infections were scattered throughout the plane between these two vertical lines, and uninfected individuals lay along the horizontal axis with arbitrary values of \(\theta\). Once thresholds for distinguishing the four classes of infection/no infection in the polar coordinate plane were established, an inverse polar coordinate transformation returned the data and the diagnosis thresholds to the Cartesian \((X,Y)\) plane (Figure 4D). This final recapitulation of the data back into the Cartesian plane illustrates the maximum magnitude, \(r_m = \max(r)\). We chose the number of bins as \(n_r = \left\lfloor \frac{r_m - r_0}{100} \right\rfloor\) (this notation indicates that we round the quantity \(\frac{r_m - r_0}{100}\) up to the nearest integer) giving bins of width approximately equal to 100 MFI units (as shown in Figure 4C). The maximum fluorescence levels obtained with Luminex FlexMap microspheres has been observed to be 25,000 MFI, and experimental blanks typically have levels less than 200 MFI. We expected uninfected individuals to have small positive background fluorescence signals clustered together around a central mean (see Methods). Therefore, we determined the first local minimum in the histogram as we increased from the lowest bin, \(r < r \leq r_0 + 100\). Heuristically, the density of points along the \(r\)-axis should peak near \(r = r_0\) and decrease smoothly as we move to successive bins, leaving the uninfected population; the density should reach a minimum before climbing again as one enters the various infected populations. Practically, this method has worked well for data sets ranging in population size from 44 to 667. For very small data sets \((n \leq 40)\) this histogram-based method should be used with caution. For further details on implementing the algorithm, see Methods. Sample code written in MATLAB is available from the authors upon request.

Having set a threshold for distinguishing infected from uninfected individuals, we then constructed a histogram of the distribution of angles \(\theta\) of the remaining, infected individuals (Figure 4C). We used 45 equally spaced bins ranging from \(\theta = 0\) to \(\theta = \pi/2\) (zero to ninety degrees, in increments of two degrees per bin). We set the threshold for the \(X-/Y+\) population (wild-type infection only) to be the first minimum in the histogram as \(\theta\) increases past the local maximum near \(\theta = 0\). The threshold for the \(X-/Y+\) population (mutant infection only) is the first minimum below the local maximum near \(\theta = \frac{\pi}{2}\) (or 90 degrees). Individuals with wild-type only infections lie scattered around a vertical line at an angle \(\theta\) that is positive (positive slope in the \((X,Y)\) plane) but close to zero. Individuals with infections carrying only the mutant allele lie scattered around a vertical line at an angle close to but less than \(\frac{\pi}{4}\) (or 90°). Individuals with mixed infections were scattered throughout the plane between these two vertical lines, and uninfected individuals lay along the horizontal axis with arbitrary values of \(\theta\). Once thresholds for distinguishing the four classes of infection/no infection in the polar coordinate plane were established, an inverse polar coordinate transformation returned the data and the diagnosis thresholds to the Cartesian \((X,Y)\) plane (Figure 4D). This final recapitulation of the data back into the Cartesian plane illustrates...
that the background cutoff lines are not parallel with either the X or Y axes, as they would have been following previous commonly practiced data analysis strategies (cf. Figure 1).

Confidence Intervals
In order to estimate the probability of classification error following polar transformation of the data, we used bootstrap resampling with replacement to establish percentage confidence interval distributions for the three thresholds (uninfected vs. infected; X+/Y- vs. X+/Y+; X-/Y+ vs. X+/Y+) [12]. With each resampled data set, we used the histogram method to determine thresholds as described above. After running the bootstrap 1,000 to 100,000 times, we determined (1 - a) percentile confidence intervals that were placed at the \( \left( \frac{a}{2} \right) \) and \( \left( 1 - \frac{a}{2} \right) \) quantiles of the bootstrap estimated thresholds (shown in Figure 4C). We used an increasing series of confidence levels, \( a_1 < a_2 < \ldots < a_n \). Each pair of confidence parameters \( a_j < a_{j+1} \) encloses a region of the \((x,y)\) plane (or equivalently, the \((r,\theta)\) plane). A hypothetical point lying in such a region would have a classification confidence between \( a_j \) and \( 1 - a_{j+1} \). For example, the pair \( a_j = .05 < a_{j+1} = .10 \) would determine a region of the plane corresponding to points with diagnosis confidence exceeding 90%, but not higher than 95%. Table 1 shows the number of points in our sample population lying within a given confidence region. The weighted average of the confidence values gives a lower bound estimate of the average diagnosis error (see Equations 1-2 under Methods). We then used these confidence intervals to obtain upper bounds on the probability that the classification of a randomly chosen
member of the population might change upon resampling. If the confidence intervals on the threshold settings were reasonably narrow, then only those individuals whose combined fluorescence measurements located them near one of the thresholds would be in danger of uncertain classification. By placing the thresholds at local minima in the density of sample points we minimized the number of individuals with ambiguous diagnoses. From these estimates, we can determine an upper bound on the probability of misdiagnosis across the entire population (denoted Pr(error)). This upper bound on the probability of error in turn gives us a lower bound on the overall confidence of our classifications (as 1-Pr(error)), shown in Table 1. For details of this calculation, please see the Methods section.

The first column of Table 1 shows bootstrap based confidence interval (CI) results for Dhfr locus 59. Out of a total population of 264 samples, six fell within a 68% confidence interval for classification but not within an 80% CI (first row of table). One fell within a 90% CI but was uncertain at the 95% confidence level (third row of table), et cetera. The last two rows of Table 1 indicate that two samples were classified with 99.9% confidence, but not better than 99.9%, and the remaining 245 samples were classified with better than 99.9% confidence as estimated by bootstrap resampling. As shown in Table 1 the assignments at each SNP locus based on the polar transform technique had bootstrap classification confidence estimates of 89% or better when averaged across the population.

### Mixed Dilution Control Experiment

In order to assess the sensitivity of the histogram segmentation based diagnostic method we used mixtures of laboratory clones (HB3, allele-T; K1, allele-A) with known genotypes to perform control LDR-FMA assays on the chr1SNP (PlasmoDB identifier, Combined-SNP: MAL1.1085 ([13]). We used a total of 34 mixtures with known DNA concentration ratios ranging from 1:1 to 99:1 (major allele:minor allele) along with a pure sample of each allele and a blank (37 samples total). The LDR-FMA assay was also performed on 264 field samples from human subjects collected in PNG. The histogram method was applied to the field data alone in order to generate diagnostic thresholds with 95% confidence intervals (see Figure 5). Subsequently the control samples were called using the thresholds obtained from the field data, and compared with the known DNA concentrations.

The results show that the histogram based method provides reliable results for a range of DNA concentration ratios (analogous to relative parasitemias for two allele types in a given patient) and breaks down once the ratio between major and minor allele concentrations becomes too large. Samples with major:minor allele ratios ranging from 1:1 to 5:1 were called correctly (as mixed infections) 100% of the time (18 out of 18 samples); samples with ratios of 9:1 or 10:1 were called correctly 67% of the time (4 out of 6 samples); both pure samples were called correctly. Mixed samples with ratios of 15:1 were called correctly 50% of the time (1 out of 2 samples) and samples with ratios of 29:1 or higher were always miscalled (as single rather than mixed infections). This performance is expected because of the mismatch binding effect described earlier: when the lower concentration allele is present in too small an amount relative to the major allele, the minor allele disappears below the advancing background signal. Fortunately the method is neverthe-

### Table 1: Locus-specific uncertainty and confidence intervals

| Confidence Intervalsa | Dhfr Locus 59 | Chr1SNP | Chr7SNP | Chr8SNP | Chr9SNP | Chr13SNP |
|-----------------------|--------------|---------|---------|---------|---------|---------|
| 0.68                  | 6            | 15      | 1       | 26      | 18      | 23      |
| 0.8                   | 0            | 9       | 15      | 30      | 1       | 3       |
| 0.9                   | 1            | 5       | 8       | 1       | 8       | 6       |
| 0.95                  | 4            | 6       | 1       | 1       | 1       | 0       |
| 0.96                  | 0            | 5       | 0       | 0       | 0       | 2       |
| 0.97                  | 1            | 0       | 3       | 0       | 6       | 0       |
| 0.98                  | 5            | 2       | 0       | 2       | 0       | 6       |
| 0.99                  | 0            | 0       | 0       | 3       | 8       | 0       |
| 0.999                 | 2            | 15      | 14      | 0       | 0       | 5       |
| > 0.999b              | 245          | 300     | 315     | 231     | 315     | 312     |
| Total Confidencec     | 0.979        | 0.954   | 0.978   | 0.899   | 0.955   | 0.944   |

aConfidence intervals for the polar transformation method as determined by bootstrap resampling with replacement. See text for details.
bData points in this category were classified with confidence exceeding 99.9% as estimated via bootstrap resampling.
cTotal confidence was determined as shown in calculating 1-Pr(error).
Comparison of histogram based threshold estimation to conventional Cartesian estimations

Following the finding that our histogram based method provides reliable results for a range of DNA concentration ratios, we can ask how well a method based on Cartesian thresholds would perform in comparison. The standard method employed in malarial SNP genotyping analysis is to set a positive infection threshold based on the distribution of fluorescence observed in an ensemble of blank controls included in the LDR/FMA assay. Typically, this threshold is set at two or three standard deviations above the mean of the blank ensemble fluorescence level.

Table 2 shows the number of individuals assigned to each of four possible states of infection with 95% or higher confidence by the polar transform histogram method, along with the number assigned to the corresponding categories using the standard Cartesian method (mean plus three standard deviations). The final row of the table lists the total number of samples reclassified when the two methods are compared. Even taking into account the number of points classified as "uncertain" by the bootstrap reclassification (an average of 31 samples/+ - 15 for six loci examined), the Cartesian method misclassifies a very significant fraction of individuals at each SNP position. This misclassification ranges from 26 to 67% of the samples at each locus, or 76 to 237 samples (Table 2).

This contrast in data analysis is apparent for the classification of infections carrying resistance-associated mutations at *dhfr* codons 59. Whereas 87 samples would be classified by conventional methods at codon 59 as infections including a mixture of parasites carrying both drug sensitive and resistant alleles, only 17 samples were classified to carry this mixed strain infection by the polar transform histogram method.
The misclassification of allele calls by conventional methods at the chr1SNP and chr9SNP are even more apparent than the dhfr codon 59 data with 226 and 237 samples respectively reclassified following the use of the polar transformation method (Table 2). This reclassification is caused by high levels of background fluorescence observed for the alleles at these loci as shown in Additional File 2: Plot of chr1SNP fluorescence data with conventional Cartesian thresholds and thresholds generated by the polar coordinate histogram method, and Additional File 3: Plot of chr9SNP fluorescence data with conventional Cartesian thresholds and thresholds generated by the polar coordinate histogram method. While genotypes at these SNP loci carry no clinical significance, these data indicate that each individual allele specific primer and associated reagent will behave differently in regards to levels of background signal. Accurate allele discrimination for genotyping *P. falciparum* infections therefore requires refined data analysis tools adapted to the intrinsic geometrical structure occurring in population data, such as the histogram based approach introduced here.

**Table 2: Reclassification of SNP allele calls by use of polar transformation compared to conventional methods**

| Genotype Status | Dhfr Locus 59 | Chr1SNP | Chr7SNP | Chr8SNP | Chr9SNP | Chr13SNP |
|-----------------|---------------|---------|---------|---------|---------|---------|
|                 | XY<sup>a</sup> | Polar<sup>b</sup> | XY<sup>a</sup> | Polar<sup>b</sup> | XY<sup>a</sup> | Polar<sup>b</sup> | XY<sup>a</sup> | Polar<sup>b</sup> | XY<sup>a</sup> | Polar<sup>b</sup> | XY<sup>a</sup> |
| Not Infected    | 127           | 137     | 77      | 104     | 92      | 92      | 70      | 28      | 66      | 95      | 92      |
| Inf. w/Allele 1 | 25<sup>c</sup> | 63      | 19      | 28      | 48      | 60      | 141     | 147     | 4       | 127     | 47      |
| Inf. w/Allele 2 | 25<sup>d</sup> | 37      | 46      | 166     | 102     | 152     | 42      | 27      | 44      | 71      | 77      |
| Mixed Infection | 87            | 17      | 215     | 24      | 115     | 28      | 41      | 34      | 243     | 36      | 141     |
| Uncertain<sup>e</sup> | -         | 10      | -       | 35      | -       | 25      | -       | 58      | -       | 28      | -       |
| Total Samples<sup>f</sup> | 264       | 357     | 357     | 294     | 357     | 357     |
| Reclassified<sup>g</sup> | 86        | 226     | 96      | 76      | 237     | 126     |

<sup>a</sup>Counts determined based on the conventional threshold of 3× standard deviations above the mean - see Figure 4A.
<sup>b</sup>Counts determined after applying polar transformation method - see Figure 4C.
<sup>c</sup>For Dhfr locus 59, allele 1 is associated with drug sensitivity.
<sup>d</sup>For Dhfr locus 59, allele 2 is associated with drug resistance.
<sup>e</sup>No samples are considered uncertain by conventional (XY) methods, as confidence intervals are not considered.
<sup>f</sup>The total number of samples genotyped at each locus.
<sup>g</sup>The number of samples whose allele calls differed between the XY and polar transformation methods.

The misclassification of allele calls by conventional methods at the chr1SNP and chr9SNP are even more apparent than the dhfr codon 59 data with 226 and 237 samples respectively reclassified following the use of the polar transformation method (Table 2). This reclassification is caused by high levels of background fluorescence observed for the alleles at these loci as shown in Additional File 2: Plot of chr1SNP fluorescence data with conventional Cartesian thresholds and thresholds generated by the polar coordinate histogram method, and Additional File 3: Plot of chr9SNP fluorescence data with conventional Cartesian thresholds and thresholds generated by the polar coordinate histogram method. While genotypes at these SNP loci carry no clinical significance, these data indicate that each individual allele specific primer and associated reagents will behave differently in regards to levels of background signal. Accurate allele discrimination for genotyping *P. falciparum* infections therefore requires refined data analysis tools adapted to the intrinsic geometrical structure occurring in population data, such as the histogram based approach introduced here.

**Conclusions**

It is to be expected that the data analysis challenges described herein will be observed in other post-PCR genotyping systems, as off-target background signals commonly increase with higher levels of PCR product amplified [17,18]. Accurate discrimination of true positive from background signal when genotyping microbial pathogens by a range of methods, including LDR-FMA and Taq Man, requires novel strategies for data analysis [19,20]. In regards to malaria, isolate differentiation is utilized for studies of parasite population diversity and structure, as well as in identification of drug resistant parasites. The reliability of genotyping methods for strain differentiation can affect the ability to monitor antimalarial drug efficacy and the presence of drug resistance mutations in a parasite population. In the future, the methods described herein can be coupled with expectation maximization approaches to further evaluate multilocus genotype and haplotype frequencies in parasite populations [21].

**Methods**

**Blood samples**

Samples evaluated in this study were part of on-going efforts to monitor *Plasmodium* species infections in the Wosera, East Sepik Province, Papua New Guinea (PNG) [22,23]. This region of northern, lowland PNG is holoendemic (parasite rate in one-year old children > 0.75 [24-26]) for malaria and all four human malaria parasite species, *P. falciparum*, *P. vivax*, *P. malariae* and *P. ovale* are observed. Informed consent was obtained from all study participants. This study was approved by the Medical Research Advisory Committee of PNG and by the Institutional Review Board for Human Investigation at University Hospitals of Cleveland, Ohio.

**P. falciparum** *(PF)* laboratory strains

*Pf* laboratory-adapted strains obtained from the Malaria Research and Reference Reagent Resource (MR4, ATCC Manassas, Virginia) included 3D7 (MRA-102), HB3
(MRA-155), K1 (MRA-159) and VS/1 (MR4-176). In vitro growth of Pf was performed as described previously [27]. Thin blood smears were fixed with 100% methanol for 30 seconds, stained with 4% Giemsa for 30 minutes, and examined by microscopy with an oil-immersion objective (100×). Parasitemia was based on the number of infected red blood cells (IRBCs)/total red blood cells (infected plus uninfected RBCs; n = 1,000).

DNA template preparation
DNA was extracted from whole blood field samples (200 μL) using the QIAamp 96 DNA Blood Kit (Qiagen, Valencia, CA). Genomic DNA was extracted from cultures (200 μL) of laboratory adapted Pf strains using the QIAamp DNA blood mini kit (Qiagen, Valencia, CA).

PCR amplification of Pf SNPs
All reactions (25 μl) were performed in a buffer containing 3 pmoles of the appropriate upstream and downstream primers, 67 mM Tris-HCl, pH 8.8, 6.7 mM MgSO₄, 16.6 mM (NH₄)₂ SO₄, 10 mM 2-mercaptoethanol, 100 μM dATP, dGTP, dCTP, and dTTP, and 2.5 units of thermostable DNA polymerase. Amplification reactions were performed in a Peltier Thermal Cycler, PTC-225 (M) Research, Watertown, MA. Specific primers and thermocycling conditions used to amplify the Pf dihydrofolate reductase (dhfr) target sequence for evaluating polymorphisms associated with pyrimethamine resistance were described in Carnevale et al [3]. Additional, presumably neutral SNPs, chosen irrespective of location or function were utilized for assessing the sensitivity of the histogram segmentation analysis and for examining the diagnostic threshold variability were amplified using the primers and conditions listed in Additional File 1: Primers and PCR amplification conditions for additional SNPs. Following PCR amplification, products were loaded on 2% Agarose gels (Amresco, Solon, OH), and electrophoresis was performed in 1× TBE buffer (8.9 mM Tris, 8.9 mM boric acid, 2.0 mM EDTA). The gels were stained for 30 min with SYBR Gold (Molecular Probes, Eugene, OR), diluted 1:10,000 in 1× TBE buffer, and DNA products were visualized on a Storm 860 using ImageQuant software (Molecular Dynamics, Sunnyvale, CA).

LDR-FMA evaluation of Pf SNPs
The methods and strategies used to perform the LDR-FMA evaluation of Pf mutations in the dhfr gene have been previously described in detail [3]. Primers for the LDR-FMA diagnosis of the additional, presumably neutral SNPs chr1SNP, chr7SNP, chr8SNP, chr9SNP, and chr13SNP are listed in Additional File 4: Ligase detection reaction primers for genotyping additional SNPs. The following brief description and summary in Figure 6 provide an overview of the three-step, post-PCR, LDR-FMA procedure.

Following PCR amplification of the gene-specific target sequences carrying the locus of interest, products were combined into a multiplex LDR (Step #1) where allele-specific upstream primers ligate to conserved sequence downstream primers. Upstream, allele-specific primers include 5′ extensions of unique "TAG" sequences. Downstream, conserved sequence primers are modified by 5′ phosphorylation and 3′ biotinylation. The 5′ ends of the LDR products receive "classification" labeling in a second multiplex (Step #2) reaction where hybridization occurs between the TAG sequences added to the allele-specific primers and anti-TAG (complementary sequence) oligonucleotide probes bound to fluorescent microspheres. Following this hybridization reaction, products are incubated (Step #3) in a solution containing streptavidin-R-phycocerythrin (SA-PE) to allow "reporter" labeling through binding to the 3′-biotin on the conserved sequence primers. Detection of doubly labeled ligation products occurs through dual fluorescence flow cytometry in the BioPlex array reader (Bio-Rad Laboratories, Hercules, CA) and leads to collection of "reporter" signal in unique allele-specific bins. Anti-TAG oligonucleotide probes bound to fluorescent microspheres (2.5 × 10⁵ beads/mL/US$25) are available from Luminex Corporation (Austin, TX).

Specific LDR primers/probes used for the dhfr locus have been previously described [3] and primers/probes for additional SNPs utilized here are listed in Additional Table 2. Individual reactions were performed in a solution (15 μL) containing 20 mM Tris-HCl buffer, pH 7.6, 25 mM potassium acetate, 10 mM magnesium acetate, 1 mM NAD+, 10 mM dithiothreitol, 0.1% Triton X-100, 10 mM (200 fmol) of each LDR probe, 1 μL of each PCR product, and 2 units of Taq DNA ligase (New England Biolabs, Beverly, MA). Reactions were initially heated at 95°C for one minute, followed by 32 thermal cycles at 95°C for 15 seconds (denaturation) and 58.0°C for 2 minutes (annealing/ligation). The multiplex LDR product (5 μL) was then added to 60 μL of hybridization solution (3 M tetramethylammonium chloride [TMAC], 50 mM Tris-HCl, pH 8.0, 3 mM EDTA, pH 8.0, 0.10% sodium dodecyl sulfate) containing 250 Luminex FlexMAP microspheres from each allelic set (total number of alleles = 9). Mixtures were heated to 95°C for 90 seconds and incubated at 37°C for 40 minutes to allow hybridization between SNP-specific LDR products and bead-labeled anti-TAG probes. Following hybridization, 6 μL of streptavidin-R-phycocerythrin (Molecular Probes, Eugene, OR) in TMAC hybridization solution (20 ng/μL) was added to the post-LDR mixture and incubated at 37°C for 40 minutes in Costar-6511M polycarbonate 96-well V-bottom plates (Corning Inc., Corning, NY). Detec-
Following PCR amplification of diallelic locus

A

Step #1 – Single tube Ligase chain reaction (LCR) to interrogate SNP

Step #2 – Denature and hybridize to microsphere-coupled oligonucleotides; incubate with SA-PE

Step #3 Detect using two color flow cytometric analysis (BioPlex Array Reader)

SNP-specific oligonucleotides with allele-specific 5' extensions

Conserved-sequence oligonucleotide with 3'-biotin

Conserved-sequence oligonucleotide with 3'-biotin bound to SA-PE

Oligonucleotides complementary to allele-specific 5' extensions, coupled to infra-red/red fluorescent microspheres

Figure 6 Overview of post-PCR, LDR-FMA diagnosis of *P. falciparum dhfr* drug resistance-associated SNPs. Allele-specific oligonucleotides include 5' "TAG" extensions that are 24 nucleotides in length. TAG sequences (n = 100), containing no G residues, have been designed to reduce potential for cross-hybridization with sequence amplified from naturally occurring target sequences. Conserved sequence oligonucleotides are 5'-phosphorylated and 3'-biotinylated. Fluorescent microsphere sets (n = 100) are embedded with varying ratios of red and infra-red fluorochromes to result in unique fluorescent "classification" signatures. Each microsphere set is pre-coupled to unique anti-TAG oligonucleotides specifically complementary to the TAG sequences. Following ligation detection and TAGami-TAG hybridization reactions, doubly labeled ligation products are detected and the "reporter" signal (R-phycocerythrin) is classified into allele-specific bins by the BioPlex array reader and BioPlex Manager 3.0 software. Data from these reactions are immediately available in Excel spreadsheets.

As a first step in evaluating background signals generated by our LDR-FMA diagnostic assays, we analyzed 70 samples from randomly selected American Red Cross blood donors who had no history of malaria exposure. Through this analysis we observed that median fluorescence intensity (MFI) LDR-FMA signals from these samples were normally distributed. From these results, conventional methods (3× standard deviations above the mean) for establishing thresholds between negative and positive fluorescence were deemed appropriate for comparison against our polar transformation method (Table 2).

Statistical analyses and graphing

All statistical analyses were performed using MATLAB version 7.7 (R2008a or b) (MathWorks Inc., Boston, MA). After transforming a set of N bivariate (x,y) fluorescence values into polar (r,θ) coordinates and forming the histogram as described above, the "first minimum after the ini-
tial maximum" in the magnitude variable was found by applying three criteria. Let \( n(r) \) denote the number of counts in the histogram centered at magnitude \( r \) and let \( \Delta r \) denote the bin width. (1) The histogram count at the minimum should be less than the counts on either side, or possibly equal to the number on the right, i.e. \( n(r-\Delta r) > n(r) \leq n(r+\Delta r) \). (2) The location of the minimum should exceed the location of the first maximum. The first maximum is required to be a local maximum and to exceed a minimum count requirement, to avoid finding spurious local max/min combinations before the true first population maximum. We used bins of size \( \Delta r = 100 \) MFI units, approximately equal to a single standard deviation of the MFI distribution for uninfected samples. We find the following heuristic to be robust in practice: assuming at least 10% of the population falls in the "uninfected" class, we expect approximately 50% of that number to fall within one standard deviation of the uninfected population mean. Therefore we use a threshold for the bin count at the "first maximum" of \( \max(8, N/20) \). (3) We impose a minimum value for the relevant "first minimum after the initial maximum." Assuming bin widths and standard deviation of MFI blank signals of 100 each, we set the bin occupancy threshold equal to twice the number of counts expected from the blank mean, if all \( N \) samples were actually uninfected. That is, we require

\[
n(r) \leq N(\text{erf}(3) - \text{erf}(2)) = 0.0466 \times N \tag{1}
\]

where \( \text{erf} \) denotes the standard error function.

After obtaining a magnitude cutoff \( (r) \) for distinguishing infected from uninfected samples, we produce a histogram of the angles \( \theta \) for all \( N_{\text{int}} \leq N \) "infected" samples, \( i.e. \) those with \( (r > r) \), in 45 bins with a width of 2 degrees ranging from zero to \( \pi/2 \) (ninety degrees). Here let \( n(\theta) \) denote the number of counts in the histogram centered at angle \( \theta \) and let \( \Delta \theta \) denote the bin width for the angle histogram. Again we apply three criteria to find the wild-type/mixed cutoff \( (\theta_{w} \text{ close to } \theta = 0) \) and the mutant/mixed cutoff \( (\theta_{m} \text{ close to } \theta = \pi/2) \). First we find the largest count in the range 0 to \( \pi/4 \) (45 degrees) or \( \pi/4 \) to \( \pi/2 \) (45 to 90 degrees), respectively. (1) Given maximum counts at \( \theta = \theta_{0} \) (the local maximum close to \( \theta = 0 \)) and \( \theta = \theta_{90} \) (the local maximum close to \( \theta = \pi/2 \)) we require \( \theta_{0} < \theta_{m} < \theta_{0} < \theta_{90} \). (2) We require that the diagnosis thresholds be placed at local minima of the histogram, i.e. \( n(\theta_{m} - \Delta \theta) > n(\theta_{m}) \leq n(\theta_{m} + \Delta \theta) \) and \( n(\theta_{90} - \Delta \theta) \geq n(\theta_{90}) < n(\theta_{90} + \Delta \theta) \). (3) In order to be an appropriate local minimum, the count at \( \theta_{m} \) or \( \theta_{90} \) should not exceed the expected number of counts for the uniform distribution of \( N_{\text{int}} \) samples over 45 bins, or \( N_{\text{int}}/45 \).

### Confidence Intervals

As described in the Results section, we estimated the probability of classification error via bootstrap resampling with replacement to establish percentage confidence interval distributions for the three thresholds (uninfected vs. infected; \( X+/Y \) vs. \( X+/Y \); \( X-/Y \) vs. \( X+/Y \)) [12]. With each resampled data set, we used the histogram method to determine thresholds. After running the bootstrap 1,000 to 100,000 times, we determined \( (1 - \alpha) \) percentile confidence intervals that were placed at the \( \left( \frac{a}{2} \right) \) and \( \left( 1 - \frac{a}{2} \right) \) quantiles of the bootstrap estimated thresholds (Figure 4C). We used these confidence intervals to obtain upper bounds on the probability that the classification of a randomly chosen member of the population might change upon resampling as follows. Let \( \rho(r, \theta) \) denote the density of signal throughout the polar plane, and let \( f(r, \theta) \) denote the classification confidence associated with any given point on the polar plane. We would like to approximate the following integral in order to bound the total probability of error by our thresholds (that is, the probability of misclassifying a sample):

\[
Pr(\text{error}) = 1 - \int_{0}^{2\pi} \int_{-\pi/2}^{\pi/2} \rho(r, \theta) f(r, \theta) r dr d\theta,
\tag{2}
\]

for \( \theta_{l} = \text{min}(\theta) \) and \( \theta_{u} = \text{max}(\theta) \) (respectively for \( r \) and \( r_{*} \)). We can rewrite this integral as:

\[
1 - Pr(\text{error}) = \frac{1}{N} \sum_{i=1}^{N} \rho(x_{i}) f(x_{i})
\tag{3}
\]

where \( x_{i} = (r_{i}, \theta_{i}) \) and \( N \) is our total sample size. If we choose a subset of confidences, such as \( \{a_{1}, a_{2}, \ldots, a_{m}\} \) for \( a_{j} \) \((0,1)\) then we can obtain an upper bound on the probability of error as the sum of the desired confidences, \( a_{p} \), multiplied by the fraction of the total sample size that lies inside those \( a_{i} \) confidence intervals. (For example, a value of \( a = 0.05 \) corresponds to a 95% confidence.) From these estimates, we obtain a lower bound on the overall confidence in our classifications (see Table 1).

### Additional material

**Additional file 1** Primers and PCR amplification conditions for additional SNPs. Primers and conditions for PCR amplification of additional SNPs utilized in assessing the sensitivity of the histogram segmentation analysis and for examining the diagnostic threshold variability.
Additional file 2 Plot of chr1SNP fluorescence data with conventional Cartesian thresholds and thresholds generated by the polar coordinate histogram method. Samples (n = 357) were genotyped at Chr1SNP using the LDR-FMA method. Allele calls were then made using both the conventional methods (3x standard deviations above the mean of known negative samples) and by the polar coordinate histogram method. Conventional thresholds are indicated by the red dotted line, and the polar thresholds are indicated by the black solid line with the black dotted line showing the 95% confidence intervals.

Additional file 3 Plot of chr9SNP fluorescence data with conventional Cartesian thresholds and thresholds generated by the polar coordinate histogram method. Samples (n = 357) were genotyped at Chr9SNP using the LDR-FMA method. Allele calls were then made using both the conventional methods (3x standard deviations above the mean of known negative samples) and by the polar coordinate histogram method. Conventional thresholds are indicated by the red dotted line, and the polar thresholds are indicated by the black solid line with the black dotted line showing the 95% confidence intervals.

Additional file 4 Ligation detection reaction primers for genotyping additional SNPs. Primers for the LDR-FMA diagnosis of additional SNPs utilized in assessing the sensitivity of the histogram segmentation analysis and for examining the diagnostic threshold variability.

Abbreviations

- SNP: Single nucleotide polymorphism
- PNG: Papua New Guinea
- LDR: ligase detection reaction
- FMA: fluorescent microsphere assay
- Pf: Plasmodium falciparum
- dhfr: dihydrofolate reductase
- dhps: dihydropterate synthetase
- pfcrt: Plasmodium falciparum chloroquine resistance transporter
- IRBC: infected red blood cell
- MFI: median fluorescence intensity
- Chr1SNP: PlasmoDB SNP Identifier CombinedSNPML11.0851
- Chr7SNP: PlasmoDB SNP Identifier CombinedSNPML7.5506
- Chr8SNP: PlasmoDB SNP Identifier CombinedSNPML8.6181
- Chr9SNP: PlasmoDB SNP Identifier CombinedSNPML9.4825
- Chr13SNP: PlasmoDB SNP Identifier CombinedSNPML13.6337

Authors’ contributions

PJT developed the mathematical and data analysis framework and advised DPK on implementation. DPK and PJT implemented the algorithms and performed the data analysis. DPK and JD performed the laboratory work and collected the LDR/FMA genotyping data. PAZ and PJT jointly supervised the overall project. JD, DPK, PAZ, and PJT wrote the manuscript. All authors read and approved the final manuscript.

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