Testing Hadronic Interaction Models with Cosmic Ray Measurements at the IceCube Neutrino Observatory

The IceCube Collaboration
(a complete list of authors can be found at the end of the proceedings)
E-mail: stef.verpoest@ugent.be

The IceCube Neutrino Observatory provides the opportunity to perform unique measurements of cosmic-ray air showers with its combination of a surface array and a deep detector. Electromagnetic particles and low-energy muons (~GeV) are detected by IceTop, while a bundle of high-energy muons (≥400 GeV) can be measured in coincidence in IceCube. Predictions of air-shower observables based on simulations show a strong dependence on the choice of the high-energy hadronic interaction model. By reconstructing different composition-dependent observables, one can provide strong tests of hadronic interaction models, as these measurements should be consistent with one another. In this work, we present an analysis of air-shower data between 2.5 and 80 PeV, comparing the composition interpretation of measurements of the surface muon density, the slope of the IceTop lateral distribution function, and the energy loss of the muon bundle, using the models Sibyll 2.1, QGSJet-II.04 and EPOS-LHC. We observe inconsistencies in all models under consideration, suggesting they do not give an adequate description of experimental data. The results furthermore imply a significant uncertainty in the determination of the cosmic-ray mass composition through indirect measurements.

Corresponding authors: Stef Verpoest1*, Dennis Soldin2, Sam De Ridder1
1 Dept. of Physics and Astronomy, University of Gent, B-9000 Gent, Belgium
2 Bartol Research Institute and Dept. of Physics and Astronomy, University of Delaware, Newark, DE 19716, USA

* Presenter

37th International Cosmic Ray Conference (ICRC 2021)
July 12th – 23rd, 2021
Online – Berlin, Germany

© Copyright owned by the author(s) under the terms of the Creative Commons Attribution-NonCommercial-NoDerivatives 4.0 International License (CC BY-NC-ND 4.0).
1. Introduction

Above 100 TeV, the flux of cosmic rays is too small to be studied adequately with balloon- or satellite-based experiments. Instead, large detector arrays at the Earth's surface are used to sample at a specific atmospheric depth the air showers produced by incoming cosmic rays interacting near the top of the atmosphere. To infer the energy and mass of the primary cosmic-ray nucleus from such measurements, one needs to rely on air-shower simulations. Important in these simulations is an accurate description of the high-energy hadronic interactions which govern the shower development in the atmosphere. Several hadronic interaction models exist that have been tuned to the data from accelerator experiments. Because these experiments are limited in the center-of-mass energy they can reach and the forwardness of the particles they can detect, these models rely on extrapolations, leading to uncertainties in interaction properties, such as cross-sections and multiplicities, which eventually leads to uncertainties in the simulated air-shower properties. This is most prominent in the muonic component of air showers, as muons are produced by decaying hadrons and thus carry information about the hadronic physics in the shower. A discrepancy between the number of muons in simulation and data has been established by a large number of experiments, and is known as the "Muon Puzzle" [1]. The potential mismodeling of the hadronic interactions furthermore complicates the determination of the mass composition in the energy range above 100 TeV, where direct measurement of cosmic rays is not possible.

The IceCube Neutrino Observatory [2] provides a unique opportunity to study these hadronic interaction models, as its combination of a detector buried deep in the Antarctic ice sheet and a surface detector array allows it to measure multiple components of air showers at once: the electromagnetic component together with both the GeV and TeV muon components. This was first used to study hadronic interaction models by examining their consistency for different composition-sensitive observables in Ref. [3], which is continued in this work.

Cosmic-ray air-shower simulations used in this work are performed with CORSIKA [4], using an average April South Pole atmospheric profile, and an observation level of 2834 m a.s.l. The high-energy hadronic interaction models considered are Sibyll 2.1 [5], QGSJet-II.04 [6], and EPOS-LHC [7]. These last two are referred to as post-LHC models, because they are tuned to LHC data, while Sibyll 2.1 is a pre-LHC model. Low-energy interactions below 80 GeV are handled by FLUKA 2011.2c [8, 9]. Before discussing the actual measurements, we highlight some differences between the high-energy models which are relevant for the case of IceCube. Fig. 1 shows the muon spectra in air showers as predicted by simulations using the different models under consideration. Both post-LHC models predict a larger number of GeV muons compared to Sibyll 2.1, while air showers simulations using QGSJet-II.04 contain more TeV muons than Sibyll 2.1, and those using EPOS-LHC contain less. Fig. 2 shows the lateral distribution functions (LDF) of photons, (anti-)electrons, and (anti-)muons for Sibyll 2.1, as well as the changes in the post-LHC models. In addition to the increase of muons over the entire distance up to 1 km away from the core, we note that the LDFs of the electromagnetic (EM) component are less steep.

\[\text{The post-LHC model Sibyll 2.3d is not included because of the absence of sufficient simulations at the time of writing.}\]
2. Cosmic ray measurements with IceCube

The IceCube Neutrino Observatory, shown in Fig. 3, consists of a surface air-shower array, IceTop [10], and a deep in-ice detector, IceCube [2], located at the geographical South Pole. IceCube instruments a volume of one cubic kilometer between depths of 1450 m and 2450 m with 5160 Digital Optical Modules (DOMs), which detect Cherenkov light generated by charged particles in the ice. The DOMs are attached to vertical strings on a triangular grid with a horizontal spacing of 125 m and a vertical spacing of 17 m. IceTop consists of 81 stations, deployed over 1 km$^2$, following approximately the same grid as the IceCube strings. The stations consist of two ice-Cherenkov tanks separated by 11 m, each containing two DOMs with different gain settings to cover a large dynamic range. The IceTop geometry is optimized for the detection of air showers from cosmic rays with primary energies between 1 PeV and 1 EeV, measuring mainly the electromagnetic and low-energy muon component of the shower. The high altitude of the array of 2835 m corresponds to an average atmospheric depth of 692 g/cm$^2$, close to the depth of shower maximum. IceTop signals are expressed in units of ‘vertical equivalent muons’ (VEM), the typical charge deposited by a single muon passing vertically through a tank [10]. Because of snow accumulation on top of the IceTop tanks, the energy at which the detector becomes fully efficient increases with time. For
the data season under consideration in this work, May 2012 to May 2013, the energy threshold is \( \log_{10}(E_0/\text{GeV}) = 6.4 \). Muons with energies \( \geq 400 \text{ GeV} \) are able to propagate through the ice and leave a signal in IceCube. Using the two detectors in coincidence allows us to measure both the low- and high-energy muons in the shower, as well as the EM component. The muons provide a strong sensitivity to the primary mass, while the EM part is crucial to reconstruct the direction and primary energy of the shower. For this study, we focus on vertical showers \( (\cos \theta > 0.95) \) with quality cuts which ensure that the shower core is contained in IceTop and the high-energy muon bundle passes through IceCube. Below we describe the reconstructions applied to the data which yield the observables used in this work.

### 2.1 IceTop LDF

The standard air-shower reconstruction method is performed on the IceTop signals. This is a maximum-likelihood technique which finds the best-fit shower direction and core position (as well as other parameters which are discussed later in this text) based on the charge and time of the signals which survive various noise removal algorithms [10]. As part of this reconstruction, the lateral distribution function given by

\[
S(R) = S_{125} \left( \frac{R}{125 \text{ m}} \right)^{-\beta-0.303 \log_{10} \left( \frac{R}{125 \text{ m}} \right)} \exp \left( \frac{-d_{\text{snow}}}{\lambda \cos \theta} \right),
\]

is fitted to the signals in the tanks, where \( S \) is the measured charge at lateral distance \( R \). The last term takes into account the attenuation of the signal due to the accumulation of snow with height \( d_{\text{snow}} \) on the tank. The snow mostly absorbs EM particles and not muons, so an effective attenuation length \( \lambda \) is used which corrects the total tank signal. It is found to be \( (2.25 \pm 0.20) \text{ m} \) for the data we consider. The two free parameters of the IceTop LDF are \( \beta \), which defines its slope, and \( S_{125} \).
the signal at 125 m. Because IceTop is located close to the depth of shower maximum, the shower size parameter $S_{125}$ is determined mainly by the abundant number of EM particles in the shower and provides an accurate estimate of the primary energy of the cosmic ray with minimal model dependence\cite{11,12}. The slope parameter $\beta$ is sensitive to the cosmic-ray mass, having lower values for heavier primaries, as shown in Fig. 4. It was verified through simulation that this dependence is a combination of two effects, relating to both the EM particles and muons measured in IceTop. First, showers from heavier primaries develop earlier in the atmosphere so that at the observation level the particles have spread out more than for lighter primaries (they have a higher shower age). Secondly, these showers also contain a larger number of muons, which further decreases the value of $\beta$, as the muon LDF is more flat than the EM LDF. The figure also shows lower values of $\beta$ in the post-LHC models, consistent with the increase of muons and flattening of the EM LDFs shown in Fig. 2.

### 2.2 Muon bundle energy loss

The reconstructed air-shower direction and position from IceTop are used as a seed track for the reconstruction of the signal deposited by the muon bundle in IceCube. Hits that are not related to this track in time and space are removed, after which a segmented reconstruction of deposited energy along the track is performed, as described in Ref. \cite{13}. The resulting energy loss profile is fitted to find the energy loss at a slant depth of 1500 m, referred to as $dE/dX_{1500}$. This parameter is strongly correlated with the number of high-energy muons in a shower\cite{12}, with heavier primaries having larger energy loss values, as shown in Fig. 4. We also see higher values of $dE/dX_{1500}$ for QGSJet-II.04 compared to Sibyll 2.1, and lower values for EPOS-LHC, consistent with the muon spectra of Fig. 1.

### 2.3 Density of GeV muons

The density of GeV muons $\rho_\mu$ in IceTop is reconstructed using the method of Refs. \cite{14,15}, which relies on the characteristic signal produced by a muon which passes vertically through a tank. Far from the shower axis, this can be used to statistically separate the muon signal from hits of other charged particles. This results in a statistical measurement of the mean density of GeV muons per event, derived over the entire data sample, at lateral reference distances of 600 m and 800 m. As shown in Fig. 4, the true muon density in simulation is higher for heavier than for lighter primaries and also higher for the post-LHC models compared to Sibyll 2.1.
3. Internal consistency of models

We test the internal consistency of air-shower simulations based on different hadronic interaction models by comparing the composition-sensitive observables described in Section 2 between experimental data and simulation. The distributions are given as a function of \( \log_{10}(S_{125}/VEM) \), using a bin width of 0.2, with a lower limit of 0.4 and an upper limit of 3 for Sibyll 2.1 and an upper limit of 2 for QGSJet-II.04 and EPOS-LHC, limited by the simulation available at the time of writing. The lower limit roughly corresponds to a primary energy of \( \log_{10}(E_0/\text{GeV}) = 6.4 \), the threshold for full efficiency, while the upper values correspond to a \( \log_{10}(E_0/\text{GeV}) \) of about 8.8 and 7.9 respectively, though the precise conversion is composition dependent. Per bin, we calculate the so-called ‘\( z \)-value’:

\[
z = \frac{x_{\text{data}} - x_p}{x_{Fe} - x_p},
\]

for each variable \( x \in \{\beta, \ln(dE/dX_{1500}), \ln(\rho_{\mu,600}), \ln(\rho_{Mu,800})\} \), where \( x_p \) and \( x_{Fe} \) are derived from proton and iron simulations based on a given hadronic model. The \( z \)-value would be 0 and 1 for a pure proton and iron composition respectively and somewhere in between for a mixed composition, while values outside this range indicate a discrepancy between data and simulation. The muon densities \( \rho_{\mu} \) are determined over the entire sample, while for the event-by-event variables \( \beta \) and \( dE/dX_{1500} \) we take the mean value in each bin. The reason to use these variables and take the logarithm for some of them, is that for variables \( x/\ln A \), Eq. (2) reduces to

\[
z = \frac{\ln A_{\text{data}}}{\ln 56}.
\]

From the Heitler-Matthews model [16], this relation is expected for the number of muons in a shower. By calculating the reconstructed \( z \)-values from helium and oxygen simulations, we see that this relation approximately holds for all variables under consideration here, as illustrated in Fig. 5.

If the simulations describe the distributions of these different variables in data correctly, the corresponding \( z \)-values are expected to overlap because they all follow the the same underlying mass composition. The resulting \( z \)-values, determined using 10% of the experimental data between May 2012 to May 2013 and simulations based on different hadronic models, are shown in Fig. 6.
Figure 6: Distribution of the different composition-sensitive observables as function of the primary energy estimator $S_{125}$ in proton-iron space as represented by the $z$-values. The error bars show the statistical uncertainty, while the bands represent the systematic uncertainties. Due to a limited availability of simulations, the results for QGSJet-II.04 and EPOS-LHC are limited to $\log_{10} S_{125}/VEM = 2$.

The systematic uncertainties on $\beta$ result from a 0.2 m uncertainty on the snow attenuation length $\lambda$ and a $\pm 3\%$ uncertainty on the calibration of the charges. For $dE/dX_{1500}$, this is accompanied by uncertainties on the scattering and absorption in the bulk ice, on the scattering in the refrozen ice surrounding the strings and on the efficiency of the DOMs, which combines into a total light yield uncertainty of $-12.5\%$ and $+9.6\%$ [12]. The systematic uncertainties for $\rho_\mu$ are dominated by the fits to signal distributions in the analysis method, as discussed in Ref. [14].

We observe that for all models the curves corresponding to the different variables increase with $S_{125}$, consistent with a composition that becomes increasingly heavy. Although the general trend is similar, there are striking inconsistencies between the variables. For Sibyll 2.1, we see that the LDF slope $\beta$ indicates a composition that is much heavier than for the low- and high-energy muon measurements, even going beyond iron, which may indicate that the predicted slope of the EM LDF is too steep. The muon measurements on the other hand overlap with eachother and give a consistent composition interpretation. For the post-LHC models, the muon density looks more proton-like in data because of the increase in muons in the simulations. For QGSJet-II.04, we notice little overlap between all considered variables, which cover a large fraction of the area between proton and iron. For EPOS-LHC, the values of $dE/dX_{1500}$ shifts up compared to Sibyll 2.1 and QGSJet-II.04, consistent with its lower number of high-energy muons. While there is acceptable agreement with $\beta$, there is a large inconsistency between the low- and high-energy muons.
4. Conclusion and Outlook

The IceCube Neutrino Observatory is able to perform unique studies of hadronic interactions in high-energy cosmic-ray physics with its capability to measure simultaneously the electromagnetic, GeV muon and TeV muon components of air showers. In this work, we presented tests of Sibyll 2.1, QGSJet-II.04, and EPOS-LHC, comparing data to proton and iron simulations for three different composition-sensitive observables. If the models give a realistic description of experimental data, the composition interpretation of all observables should be consistent. However, we observe inconsistencies between different components in the models considered, notably between the LDF slope and the low-energy muons in all models, and the low- and high-energy muons in the post-LHC models. These inconsistencies furthermore make it challenging to unambiguously determine the mass composition of cosmic rays through indirect measurements.

Inclusion of more data, increased availability of simulations, and a better understanding of systematics will advance the precision of the tests we presented. Future work improving measurements of low- and high-energy muons will provide additional input relevant for the understanding of air shower physics. The extension of the Observatory with a larger in-ice detector and new surface detectors [17–19] will further allow to expand this work with more complementary measurements.

References

[1] H. P. Dembinski et al. *EPJ Web Conf.* **210** (2019) 02004.
[2] IceCube Collaboration, M. G. Aartsen et al. *JINST* **12** no. 03, (2017) P03012.
[3] S. De Ridder, E. Dvorak, and T. Gaisser *PoS ICRC2017* (2017) 319.
[4] D. Heck et al., CORSIKA: A Monte Carlo code to simulate extensive air showers, *Report FZKA 6019, Forschungszentrum Karlsruhe*, 1998.
[5] E.-J. Ahn, R. Engel, T. K. Gaisser, P. Lipari, and T. Stanev *Phys. Rev. D* **80** (2009) 094003.
[6] S. Ostapchenko *Phys. Rev. D* **83** (2011) 014018.
[7] T. Pierog, I. Karpenko, J. M. Katzy, E. Yatsenko, and K. Werner *Phys. Rev. C* **92** no. 3, (2015) 034906.
[8] T. Böhlen et al. *Nuclear Data Sheets* **120** (2014) 211–214.
[9] G. Battistoni et al. *Annals of Nuclear Energy* **82** (2015) 10–18.
[10] IceCube Collaboration, R. Abbasi et al. *Nucl. Instrum. Meth. A* **700** (2013) 188–220.
[11] IceCube Collaboration, M. G. Aartsen et al. *Phys. Rev. D* **88** no. 4, (2013) 042004.
[12] IceCube Collaboration, M. G. Aartsen et al. *Phys. Rev. D* **100** no. 8, (2019) 082002.
[13] IceCube Collaboration, M. G. Aartsen et al. *JINST* **9** (2014) P03009.
[14] IceCube Collaboration, J. G. Gonzalez *EPJ Web Conf.* **208** (2019) 03003.
[15] IceCube Collaboration, D. Soldin *PoS ICRC2021* (these proceedings) 342.
[16] J. Matthews *Astropart. Phys.* **22** (2005) 387–397.
[17] IceCube-Gen2 Collaboration, M. G. Aartsen et al. *J. Phys. G* **48** no. 6, (2021) 060501.
[18] IceCube Collaboration, A. Haungs *EPJ Web Conf.* **210** (2019) 06009.
[19] IceCube Collaboration, L. Paul, M. Schaufel, and M. Plum *PoS ICRC2021* (these proceedings) 276.
Hadronic interaction model Studies with IceCube

16 Dept. of Physics and Institute for Global Prominent Research, Chiba University, Chiba 263-8522, Japan
17 Department of Physics, Loyola University Chicago, Chicago, IL 60660, USA
18 Dept. of Physics and Astronomy, University of Canterbury, Private Bag 4800, Christchurch, New Zealand
19 Dept. of Physics, University of Maryland, College Park, MD 20742, USA
20 Dept. of Astronomy, Ohio State University, Columbus, OH 43210, USA
21 Dept. of Physics and Center for Cosmology and Astro-Particle Physics, Ohio State University, Columbus, OH 43210, USA
22 Niels Bohr Institute, University of Copenhagen, DK-2100 Copenhagen, Denmark
23 Dept. of Physics, TU Dortmund University, D-44221 Dortmund, Germany
24 Dept. of Physics and Astronomy, Michigan State University, East Lansing, MI 48824, USA
25 Dept. of Physics, University of Alberta, Edmonton, Alberta, Canada T6G 2E1
26 Erlangen Centre for Astroparticle Physics, Friedrich-Alexander-Universität Erlangen-Nürnberg, D-91058 Erlangen, Germany
27 Physik-department, Technische Universität München, D-85748 Garching, Germany
28 Département de physique nucléaire et corpusculaire, Université de Genève, CH-1211 Genève, Switzerland
29 Dept. of Physics and Astronomy, University of Gent, B-9000 Gent, Belgium
30 Dept. of Physics and Astronomy, University of California, Irvine, CA 92697, USA
31 Karlsruhe Institute of Technology, Institute for Astroparticle Physics, D-76021 Karlsruhe, Germany
32 Karlsruhe Institute of Technology, Institute of Experimental Particle Physics, D-76021 Karlsruhe, Germany
33 Dept. of Physics, Engineering Physics, and Astronomy, Queen’s University, Kingston, ON K7L 3N6, Canada
34 Dept. of Physics and Astronomy, University of Kansas, Lawrence, KS 66045, USA
35 Department of Physics and Astronomy, UCLA, Los Angeles, CA 90095, USA
36 Department of Physics, Mercer University, Macon, GA 31207-0001, USA
37 Dept. of Astronomy, University of Wisconsin–Madison, Madison, WI 53706, USA
38 Dept. of Physics and Wisconsin IceCube Particle Astrophysics Center, University of Wisconsin–Madison, Madison, WI 53706, USA
39 Institute of Physics, University of Mainz, Staudinger Weg 7, D-55099 Mainz, Germany
40 Department of Physics, Marquette University, Milwaukee, WI, 53201, USA
41 Institut für Kernphysik, Westfälische Wilhelms-Universität Münster, D-48149 Münster, Germany
42 Bartol Research Institute and Dept. of Physics and Astronomy, University of Delaware, Newark, DE 19716, USA
43 Dept. of Physics, Yale University, New Haven, CT 06520, USA
44 Dept. of Physics, University of Oxford, Parks Road, Oxford OX1 3PU, UK
45 Dept. of Physics, Drexel University, 3141 Chestnut Street, Philadelphia, PA 19104, USA
46 Physics Department, South Dakota School of Mines and Technology, Rapid City, SD 57701, USA
47 Dept. of Physics, University of Wisconsin, River Falls, WI 54022, USA
48 Dept. of Physics and Astronomy, University of Rochester, Rochester, NY 14627, USA
49 Department of Physics and Astronomy, University of Utah, Salt Lake City, UT 84112, USA
50 Oskar Klein Centre and Dept. of Physics, Stockholm University, SE-10691 Stockholm, Sweden
51 Dept. of Physics and Astronomy, Stony Brook University, Stony Brook, NY 11794-3800, USA
52 Dept. of Physics, Sungkyunkwan University, Suwon 16419, Korea
53 Institute of Basic Science, Sungkyunkwan University, Suwon 16419, Korea
54 Dept. of Physics and Astronomy, University of Alabama, Tuscaloosa, AL 35487, USA
55 Dept. of Astronomy and Astrophysics, Pennsylvania State University, University Park, PA 16802, USA
56 Dept. of Physics, Pennsylvania State University, University Park, PA 16802, USA
57 Dept. of Physics and Astronomy, Uppsala University, Box 516, S-75120 Uppsala, Sweden
58 Dept. of Physics, University of Wuppertal, D-42119 Wuppertal, Germany
59 DESY, D-15738 Zeuthen, Germany
60 Università di Padova, I-35131 Padova, Italy
61 National Research Nuclear University, Moscow Engineering Physics Institute (MEPhI), Moscow 115409, Russia
62 Earthquake Research Institute, University of Tokyo, Bunkyo, Tokyo 113-0032, Japan

Acknowledgements

USA – U.S. National Science Foundation-Office of Polar Programs, U.S. National Science Foundation-Physics Division, U.S. National Science Foundation-EPSCoR, Wisconsin Alumni Research Foundation, Center for High Throughput Computing (CHTC) at the University of Wisconsin–Madison, Open Science Grid (OSG), Extreme Science and Engineering Discovery Environment (XSEDE), Frontera computing project at the Texas Advanced Computing Center, U.S. Department of Energy-National Energy Research Scientific Computing Center, Particle astrophysics research computing center at the University of Maryland, Institute for Cyber-Enabled Research at Michigan State University, and Astroparticle physics computational facility at Marquette University; Belgium – Funds for Scientific Computing Center, Particle astrophysics research computing center at the University of Maryland, Institute for Cyber-Enabled Research at Michigan State University, and Astroparticle physics computational facility at Marquette University; Belgium – Funds for Scientific Computing Center, Particle astrophysics research computing center at the University of Maryland, Institute for Cyber-Enabled Research at Michigan State University, and Astroparticle physics computational facility at Marquette University; Belgium – Funds for Scientific Computing Center, Particle astrophysics research computing center at the University of Maryland, Institute for Cyber-Enabled Research at Michigan State University, and Astroparticle physics computational facility at Marquette University; Belgium – Funds for Scientific Computing Center, Particle astrophysics research computing center at the University of Maryland, Institute for Cyber-Enabled Research at Michigan State University, and Astroparticle physics computational facility at Marquette University; Belgium – Funds for Scientific Computing Center, Particle astrophysics research computing center at the University of Maryland, Institute for Cyber-Enabled Research at Michigan State University, and Astroparticle physics computational facility at Marquette University; Belgium – Funds for Scientific Computing Center, Particle astrophysics research computing center at the University of Maryland, Institute for Cyber-Enabled Research at Michigan State University, and Astroparticle physics computational facility at Marquette University.
Research Council; Canada – Natural Sciences and Engineering Research Council of Canada, Calcul Québec, Compute Ontario, Canada Foundation for Innovation, WestGrid, and Compute Canada; Denmark – Villum Fonden and Carlsberg Foundation; New Zealand – Marsden Fund; Japan – Japan Society for Promotion of Science (JSPS) and Institute for Global Prominent Research (IGPR) of Chiba University; Korea – National Research Foundation of Korea (NRF); Switzerland – Swiss National Science Foundation (SNSF); United Kingdom – Department of Physics, University of Oxford.