ABSTRACT

We study the K-correction for the case of emission lines formed in the X-ray–illuminated atmosphere of a Roche lobe–filling star. We compute the K-correction as a function of the mass ratio q and the disk flaring angle α using a compact binary code in which the companion’s Roche lobe is divided into 105 resolution elements. We also study the effect of the inclination angle in the results. We apply our model to the case of the neutron star low-mass X-ray binary X1822–371 (V691 CrA), where a K-emission velocity $K_{em} = 300 \pm 8 \text{ km s}^{-1}$ has been measured by Casares et al. Our numerical results, combined with a previous determination of system parameters, yields $1.61 M_\odot \leq M_{NS} \leq 2.32 M_\odot$ and $0.44 M_\odot \leq M_\odot \leq 0.56 M_\odot$ for the two binary components (i.e., $0.24 \leq q \leq 0.27$), which provide compelling evidence for a massive neutron star in this system. We also discuss the implications of these masses into the evolutionary history of the binary.

Subject headings: accretion, accretion disks --- binaries: close --- stars: individual (X1822–371) --- X-rays: stars

1. INTRODUCTION

Low-mass X-ray binaries (LMXBs) are interacting binaries in which a low-mass star transfers matter onto a neutron star (NS) or black hole (e.g., Charles & Coe 2006). There are ~200 bright ($L_X \approx 10^{36}–10^{38} \text{ ergs s}^{-1}$) LMXBs in the Galaxy, and most of them harbor NSs, as implied by the detection of X-ray bursts/pulsations. About 20 of these have period determinations, but only in very few cases (e.g., Cyg X-2: Casares et al. 1998; Orosz & Kuulkers 1999; V395 Car: Shahbaz et al. 2004; Jonker et al. 2003) does a full orbital solution and mass determination exist, respectively, by fitting sine waves to the He i radial velocity curves. However, as Jonker et al. pointed out, the spectroscopic $T_0$ is delayed by 0.1P orb with respect to the photometric eclipses and pulsar ephemeris, and hence asymmetric irradiation of the Roche lobe needs to be invoked.

In Casares et al. (2003, hereafter C03), the first unambiguous detection of the donor star is reported using the N iii $\lambda4640$ Bowen emission line with a velocity amplitude of $K_{em} = 300 \pm 8 \text{ km s}^{-1}$. The phasing of the N iii velocity curve is perfectly consistent with the pulsar ephemeris with no need for ad hoc asymmetric illumination effects. Furthermore, they show that the He i absorptions come from the accretion stream and not from the companion star. This naturally explains the phase offset with the pulsar ephemeris observed in previous works.

However, the N iii Bowen emission line is excited on the inner hemisphere of the donor star and only provides a lower limit to the true $K_2$-velocity. Narrow high-excitation emission lines originating from the companion star have also been detected in the prototypical LMXB Sco X-1 (Steeghs & Casares 2002) and in the black hole X-ray transient GX 339-4 during its 2002 outburst (Hynek et al. 2003). These narrow features are strongest in the Bowen blend, a set of resonant emission lines (mainly C iii and N iii $\lambda4640$) excited by photoionization and the Bowen mechanism (McCintock et al. 1975). The Roche lobe–shaped donor star intercepts the energetic photons from the inner accretion disk resulting in the observed optical emission lines from its surface. The Doppler motion of these lines traces the orbit of the companion star and provides the first reliable binary parameters in persistent LMXBs. However, the secondary is not uniformly illuminated by the ionizing photons, and therefore, the radial velocity curve of the sharp features traces the motion of the reprocessed light center rather than the true center of mass of the star.

In this paper we model the deviation between the reprocessed light center and the center of mass of a Roche lobe–filling star (the so-called K-correction) in a persistent LMXB, including screening effects by a flared accretion disk. We apply our simulations to the case of X1822–371 and conclude that it must contain a massive NS with $M_{NS} \sim 1.61–2.32 M_\odot$, for any possible value of the disk flaring angle.
2. THE “K-CORRECTION” FOR EM (EMISSION) LINES IN THE IRRADIATED FACE

The K-correction for radial velocity curves derived from absorption lines formed on the companion’s photosphere was presented by Wade & Horne (1988, hereafter WH88). In this case, absorption lines are quenched in the heated face, and hence the observed K-velocity provides only an upper limit to the real $K_2$, i.e., the true velocity of the center of mass of the companion star. Here, we study the K-correction for the case of irradiated-induced spectral lines originating from the heated face of the donor star, which is opposite to the case presented in WH88. This problem was first addressed by Horne & Schneider (1989, hereafter HS89), but it was only applied to the particular case of nova V1500 Cyg without screening effects by a possible accretion disk. In addition, Beuermann & Thomas (1990) studied this problem for the case of the cataclysmic variable IX Velorum. They considered only two different accretion disk angles together with the orbital parameters of this binary. In this paper we tackle the problem in a general approach and derive a K-correction expression for all possible $q$-values and obscuring disk elevations.

Following the prescription of HS89, the light center ($l_c$) of the emission-line region is given by $l_c = a_2 - d$, where $d$ represents the light-center displacement from the center of mass of the donor star and $a_2 = a/(1 + q)$ is the distance between the center of mass of the companion and the center of mass of the system; $q = M_2/M_1$ is the mass ratio, and $a$ is the binary separation. Using this nomenclature, the difference between the $K_2$ and the observed emission-line velocity ($K_{em}$) is

$$\Delta K = K_2 - K_{em} = K_2 \frac{d}{a_2},$$

and therefore

$$K_2 = K_{em} \frac{1 - d[(1 + q)/a]}{1 - f(1 + q)}, \quad \text{(1)}$$

where $f$ is a dimensionless factor that represents the displacement of the emission light center from the center of mass of the companion in units of $a$. In the limit case where the emission lines are formed at the inner Lagrange point ($L_1$),

$$f = \frac{b_2}{a} \sim 0.5 + 0.227 \log q$$

(Plavec & Kratochvil 1964), where $b_2$ is the distance between $L_1$ and the center of mass of the companion star. On the other hand, we can consider the extreme case where the emission line comes from the irradiated point with maximum radial velocity. This point is located at the limb of the irradiated region and holds an opening angle $\alpha_M$ above the plane of the binary.\(^3\) This is the highest possible angle for the companion to be irradiated, and it has been tabulated by R. Pennington in Table A3 of the Appendix in Pringle & Wade (1985). An approximate analytical expression, as a function of $q$, is provided by the Paczynski (1971) equation:

$$\sin \alpha_M \simeq \frac{R_2}{a} \simeq 0.462 \left( \frac{q}{1 + q} \right)^{1/3}. \quad \text{(2)}$$

\(^3\) Note that for this case to work, the accretion disk must screen the rest of the inner face of the donor.

Then, if we assume that the Roche lobe is spherical (which is a good approximation when we are far from $L_1$), it is easy to show that the minimum $f$ displacement is given by $\sim \sin^2 \alpha_M$. Therefore, in any possible situation $f$ will always be constrained between these two cases, i.e.,

$$0.5 + 0.227 \log q > f > \sin^2 \alpha_M.$$  

These limits are presented in Figure 1, plotted as dashed lines. Here we have used the exact $\alpha_M$ values calculated by our code (see below), which obviously coincide with the ones tabulated by R. Pennington.

However, the upper limit obtained is purely theoretical, since $L_1$ will never be the only irradiated point of the donor star. A more realistic upper limit can be obtained by simulating emission lines formed by isotropic irradiation on the inner hemisphere of the companion in a Roche lobe geometry. We have divided the Roche lobe–filling star in 10\(^3\) triangular tiles of equal surface. The flux from the X-ray source that is reprocessed in each tile will be given by

$$F_r \sim \frac{F_X(1 - \varepsilon) \cos \theta_X}{P_r^2} a_t,$$

where $F_X$ is the X-ray flux emitted by the compact object, $a_t$ is the area of the tile, $r$ is the distance between the tile and the center of mass of the primary star, $\cos \theta_X$ is the projection factor of the tile as seen by the X-ray source, and $\varepsilon$ is the albedo. The total reprocessed emission-line flux seen by a distant observer is obtained by integrating $F_r \cos \theta_p P_r$ over the Roche lobe geometry, where $\cos \theta_p$ is the projection factor of each irradiated tile as seen by the observer and $P_r$ represents a local Gaussian profile. We have not included limb-darkening effects in the simulation, because these are expected to be negligible in the optically thin case that we are considering here. To test this hypothesis, we have also included in our simulations a linearized limb darkening, appropriate to the continuum (i.e., optically thick case), and found that it had no impact on the results.

Radial velocity curves were subsequently computed by measuring the position of the maxima in the synthetic profiles (which
are not symmetric), and $K_{em}$ is determined from the maxima of the radial velocity curves. Therefore, for a given $K_2$ equation (1) gives the $f$-values as a function of $q$. These values, as expected, are not found to depend on either $\varepsilon$ or $F_X$. The synthetic $f(q)$ curve is plotted in Figure 1 as a solid line, and a fourth-order polynomial fit (which is accurate to better than 1%) to this curve yields

$$f(\alpha = 0^\circ) = 0.116 + 0.946q - 1.947q^2 + 2.245q^3 - 1.002q^4.$$ 

Then, the real value of $f$ will be constrained between these two limits, i.e., $f(\alpha = 0^\circ) > f > \sin^2\alpha M_H$, and will depend on the size of the companion (i.e., the mass ratio) and the height of the accretion disk rim obscuring the heated star.

In a second step, we have incorporated shadowing effects by a flared and opaque accretion disk with an opening angle $\alpha$ independent of azimuth. Figure 2 presents the synthetic radial velocity curves computed for four different disk-obscuring angles. The plot shows how the radial velocity curves start to deviate from pure sine wave functions when $\alpha$ decreases. Because the velocity amplitude is strongly dependent on $\alpha$, so does the $K$-correction. Therefore, using our binary code we have computed the relation between the ratio $K_{em}/K_2$ and $q$ for different values of the flaring angle $\alpha$, and these are plotted in Figure 4 as solid lines.

In Figure 3 we also explore the effect of the inclination angle in the shape of the radial velocity curve. This plot shows that the morphology of the radial velocity curves clearly depends on the inclination angle, and hence $K_{em}/K_2$ could be a function of this parameter as well. Using our numerical model, we have found that (in the most extreme cases when $q > 0.6$) $K_{em}/K_2$ can be $\sim 10\%$ smaller for low inclination angles than for $i = 90^\circ$. To illustrate the effect of the inclination angle, we have also computed the $K$-correction for $i = 40^\circ$ and different $\alpha$-values, and these are overplotted in Figure 4 as dash-dotted lines.

The synthetic $K$-corrections produced by the numerical code are very smooth and can be well described by fourth-order polynomial fits. Table 1 lists the coefficients of the fits for the two values of the inclination considered and different opening angles (from $0^\circ$ to $18^\circ$) that cover the typical values observed in XRBs and cataclysmic variables. These fits are accurate to better than 1% between $q \sim 0.05$ and 0.83. For the case of intermediate inclinations, the interpolated solution between $i = 90^\circ$ and $40^\circ$ is accurate to $\leq 2\%$. For $i \leq 40^\circ$ the $i = 40^\circ$ value gives also a very good approximation ($< 2\%$). Note that the value of $K_{em}/K_2$ obtained for $i = 90^\circ$ yields a secure lower limit to the masses of the binary components for all possible cases. For intermediate $\alpha$- and $i$-values one needs to interpolate the $K$-correction solutions and not the coefficients.

Hence, for a given mass ratio $q$, the $K$-correction is provided by

$$\frac{K_{em}}{K_2} \cong N_0 + N_1q + N_2q^2 + N_3q^3 + N_4q^4.$$ 

Note that, since the $K$-correction is only meaningful if $\alpha \leq \alpha_M$ (otherwise the companion will be completely shadowed by the disk), equation (2) sets a lower limit to $q$ for each $\alpha$ (see Fig. 4). For this reason the first values of $q$ considered in the fits for $\alpha = 10^\circ, 12^\circ, 14^\circ, 16^\circ,$ and $18^\circ$ are $q = 0.1, 0.15, 0.26, 0.4,$ and 0.58, respectively. As a test, we have computed the $K$-correction.
for the binary parameters of nova V1500 Cyg and obtain $K_{em}/K_2 = 0.64$, in excellent agreement with HS89.

3. THE K-CORRECTION FOR X1822−371

Now we can apply our computed K-correction to the case of X1822−371 and derive the masses for the two components. In C03 a $K_{em} = 300 \pm 8$ km s$^{-1}$ was reported through the detection of the N III λ4640 Bowen emission line arising from the companion star. This value, combined with the previous determination of the inclination angle and the pulsar’s radial velocity curve, yields absolute lower limits of $M_1 \geq 1.14 M_\odot$ and $M_2 \geq 0.36 M_\odot$, assuming $K_2 \geq K_{em}$ (see C03).

On the other hand, the mass function equation can be expressed as

$$M_l = \frac{(K_1/q)^3 P (1 + q)^2}{2\pi G \sin^3 i},$$

where $P$ is the orbital period and $G$ is the gravitational constant. In the case of X1822−371, where $i$ and $K_1$ are known, this equation provides a direct relation between $q$ and $M_l$. Therefore, this can be combined with our synthetic K-correction curves to yield $K_{em}$-$M_l$ relations for different disk opening angles $\alpha$.

C03 obtained $K_{em} = 300 \pm 8$ km s$^{-1}$ by fitting the N III λ4640 spot in the Doppler map with a two-dimensional Gaussian function. Instead, we have computed the centroid of the spot intensity distribution and obtain a more conservative value of $K_{em} = 300 \pm 15$ km s$^{-1}$, which we prefer since it does not impose any model to the fit. In order to test whether the K-correction derived by our model can be used to correct the $K_{em}$ value extracted from the Doppler tomography, we have simulated irradiated profiles (using our derived parameters of X1822−371; see below) for the orbital phases of the C03 observations. These were smeared according to the exposure times used and subsequently degraded to the spectral resolution of the observations. Finally, we added noise to reproduce the observed spectra. A Doppler map was then computed, and the centroid of the spot was found to be in excellent agreement, within the errors, with the value above. Furthermore, we note that the same $K_{em}$ was obtained by Steeghs & Casares (2002) in Sco X-1 from the radial velocity curve and Doppler tomography.

Under the assumption that the Bowen emission lines are formed on the critical Roche lobe of the companion, the detection of this emission at $K_{em} = 300 \pm 15$ km s$^{-1}$ directly yields $M_{NS} \gg 1.35 M_\odot$ and $M_2 \gg 0.4 M_\odot$ through the geometric limit $f > \sin^2 \alpha M_l$. However, realistic mass determinations require the knowledge of the disk rim elevation obscuring the companion; de Jong et al. (1996) derived a mean disk opening angle of $\alpha \sim 12^\circ$ by studying the effects of X-ray reprocessing in LMXBs. This value was also derived by HM89 for the highest disk structure (i.e., the bulge at phase $\sim 0.8$) in X1822−371 by modeling simultaneous optical and X-ray EXOSAT light curves. However, in HN01 a higher angle of $\alpha \sim 14^\circ$ is obtained by fitting X-ray Rossi X-Ray Timing Explorer and Advanced Satellite for Cosmology and Astrophysics (RXTE + ASCA) light curves. These estimates correspond to the disk elevation at the phase of the bulge and therefore must be treated as upper limits to the height of the disk rim obscuring the companion, which is constrained to $-0.04 \leq \phi \leq 0.04$. In any case, these opening angles are expected to be, in general, only slightly higher than the real ones, and hence we have calculated the $K_{em}$-$M_l$ relation for both disk thicknesses as shown in Figure 5. If we take into account the opening angles considered, the inclination uncertainty, and the errors in the observed $K_{em}$, Figure 5 shows that the mass of the NS is constrained to the range

$$1.61 M_\odot \leq M_{NS} \leq 2.32 M_\odot.$$

We would like to remark that this provides a conservative lower limit to $M_{NS}$. If the accretion disk were thinner, then the mass would be even higher. For instance, if $\alpha = 0^\circ$ (i.e., no disk), $M_{NS}$ must be $\geq 3 M_\odot$ in order to reproduce the observed $K_{em}$ at $\alpha \sim 12^\circ$.
\( \approx 300 \text{ km s}^{-1} \). Besides, since the NS mass and the mass ratio are related by the mass function, we obtain \( 0.24 \leq q \leq 0.27 \), which leads to

\[ 0.44 M_\odot \leq M_2 \leq 0.56 M_\odot. \]

4. DISCUSSION

The detection of irradiated-induced emission lines originating from the heated face of the companion star can yield important restrictions to the mass of the binary components; \( K_{\text{em}} \) contains intrinsic information about the companion’s regions responsible for reprocessing the X-ray/UV radiation. Since the orbital parameters of X1822–371 are tightly constrained, the key missing information for a realistic simulation are the structures present between the companion and the X-ray source. Our simple model only takes into account screening effects by a flared accretion disk. However, the presence of a disk corona scattering the X-rays/EUV radiation might modify the results of our simulations, since irradiating photons could reach (otherwise obscured) regions of the Roche lobe with lower velocities. Consequently, the scattered radiation is expected to push the \( K \)-correction to lower values and hence the NS to higher masses. As a test we have included emission from a “corona” that has been roughly simulated by five X-ray spots symmetrically distributed around the compact object at a distance of 0.2\( r \) (i.e., the corona radii derived in HN01). The integrated flux of this simplified corona was scaled to be 1% of the accretion luminosity, i.e., \( 10^{38} \) ergs s\(^{-1}\) for an assumed compact object luminosity of \( 3 \times 10^{37} \) ergs s\(^{-1}\). Our observed masses, orbital period, and \( \dot{M} \) in HN01 proposed that X1822–371 is an ADC source, we only see X-rays scattered by the corona, and there are only rough estimates of the true luminosity. For instance, Jonker & van der Klis (2001) derived \( L_X \sim (2-4) \times 10^{37} \) ergs s\(^{-1}\) from the spin-up and constraints to the magnetic field. This, in turn, implies \( \dot{M}_1 \sim 10^{-9} M_\odot \) yr\(^{-1}\), i.e., 1 order of magnitude lower than predicted from \( \dot{P} \). However, this discrepancy could be reconciled if \( \dot{M}_1 \) were driven by secular changes and did not reflect \( \dot{P} \) (e.g., magnetic cycles in the companion; Hellier et al. 1990).

HN01 proposed that X1822–371 might have had an evolutionary history similar to Cyg X-2 (Podsiadlowski & Rappaport 2000; Kolb et al. 2000), in which the system descended from an intermediate-mass X-ray binary (IMXB) with \( q \gg 1 \). In this scenario the secondary must have lost more than \( \sim 1 M_\odot \) from its outer layers in order to reach its current mass, and it should expose CNO-processed material from the inner layers. Unfortunately, the companion star is not directly detected spectroscopically, and hence the spectral type and the history evolution are unconstrained. However, the emission-line spectra reported in C03 seem to show “normal-strength” \( \text{C} \text{m} \) lines within the Bowen blend and also a strong O \( \text{vi} \) at 13811. Our observed masses, orbital period, and \( \dot{M}_1 \) could be accommodated by some IMXB evolutionary sequences with an initial companion’s mass and orbital period of \( \sim 3.5 M_\odot \) and \( \sim 20 \) hr, respectively (Ph. Podsiadlowski 2005, private communication). The currently observed \( q < 0.25 \) implies that X1822–371 must have long passed the thermal mass transfer phase, and its evolution should be currently driven by magnetic braking phase with \( P < 0 \) to sustain mass transfer, in clear contradiction to the observed \( \dot{P} > 0 \). Alternatively, mass transfer could be sustained by X-ray irradiation, as suggested in Pfahl et al. (2003). A fundamental test of the evolutionary history of X1822 will be to perform new high-resolution optical and UV spectroscopy to search for evidence of CNO-processed material (e.g., XTE J1118+480; Haswell et al. 2002).

In the case of X1822–371, with \( P_{\text{orb}} = 5.57 \), we obtain \( \dot{P} \approx 3.7 \) g cm\(^{-3}\). This value is consistent with a 0.5 \( M_\odot \) M0 main-sequence (MS) star (Cox 2000), and it is in excellent agreement with our derived mass. We also note that a 0.5 \( M_\odot \) MS star would not have evolved in a Hubble time. However, if we assume that the NS at formation was \( \sim 1.4 M_\odot \), then it must have accreted \( \sim 0.5 M_\odot \) from the companion to reach its current \( \sim 1.9 M_\odot \), and hence it must have had at least \( \geq 1 M_\odot \) at the onset of the mass transfer phase.

Faulkner et al. (1972) showed that the mean density of a Roche lobe–filling companion star is determined solely by the binary period \( P \):

\[ \bar{\rho} \approx 113 P_{\text{hr}}^{-2} \text{ g cm}^{-3}. \]

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