Photonic simulation of topological excitations in metamaterials

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Condensed matter systems with topological order and metamaterials with left-handed chirality have attracted recently extensive interests in the fields of physics and optics. So far the topological order and chirality of electromagnetic wave are two independent concepts, and there is no work to address their connection. Here we propose to establish the relation between the topological order in condensed matter systems and the chirality in metamaterials, by mapping explicitly Maxwell’s equations to the Dirac equation in one dimension. We report an experimental implement of the band inversion in the Dirac equation, which accompanies change of chirality of electromagnetic wave in metamaterials, and the first microwave measurement of topological excitations and topological phases in one dimension. Our finding provides a proof-of-principle example that electromagnetic wave in the metamaterials can be used to simulate the topological order in condensed matter systems and quantum phenomena in relativistic quantum mechanics in a controlled laboratory environment.

The Dirac equation provides a description of relativistic quantum mechanics for an elementary spin-1/2 particle⁴,⁵, which predates the discovery of positron, an anti-particle of electron in high energy physics⁶, and also has extensive applications in condensed matters such as graphene⁴,⁵ and topological insulators⁶,⁷. Recent years it is realized that it is a key to understand topological phases from one to three dimensions and from insulators to superconductors or superfluids⁸. On the other hand, Maxwell’s equations form the foundations of classical electrodynamics and modern optics. Modern techniques and material sciences make it possible to precisely control photonic transport in metamaterials, such as negative refraction⁹,¹⁰, electromagnetic cloaking¹¹,¹², structure-induced coherence¹³–¹⁶, and mimicking photonic black holes¹⁷. It will be of great interest and importance to link the metamaterials to topological phenomena in condensed matters and the relativistic quantum mechanics. In fact, several proposals have been reported to generate photonic counterparts of quantum Hall edge states¹⁸–²⁰ and topological insulators²¹ in photonic lattice structures. In these studies, a hexagonal or square lattice was designed to obtain the Dirac point, near which an effective Hamiltonian as well as a Dirac equation was derived in the long wave limit and the topological invariant can be calculated. This demonstrates a link between the topological insulators and electromagnetic media.

Here we demonstrate an alternative approach to simulate topological excitations by mapping explicitly Maxwell’s equations to the Dirac equation in one dimension by employing subwavelength metamaterials. The remarkable property of metamaterials lies in their flexibility to have controllable signs and magnitudes of their effective permittivity and permeability. If the permittivity and permeability are simultaneously negative, electromagnetic waves in such metamaterials show left-handed chirality⁹,¹⁰. So far there is no work to address the connection between the topological order and the chirality. We find that the one-dimensional (1D) Maxwell’s equations can be written in the compact form which has the identical mathematical structure of the Dirac equation, and consequently perform a proof-of-principle photonic simulation of the Dirac equation in metamaterials by means of the full wave numerical simulation and microwave experiment of transmission line. By tailoring the electromagnetic responses of metamaterials, we successfully implement the band inversion of the Dirac equation. It is noted that the band inversion accompanies change of the chirality of electromagnetic wave in metamaterials from the right-handed to left-handed triad and vice versa, which determines a matter-antimatter correspondence in the relativistic quantum mechanics. For the first time we establish possible relation of the chirality of electromagnetic wave and the topological order. Furthermore we utilize designing metamaterials to observe experimentally the topological phases and excitations in one dimension. This paves the way to investigate the topological phenomena in condensed matters and the Dirac-like particles in high-energy physics in a
photonic simulator. Meanwhile, we can also make use of the solutions of the Dirac equation to understand exotic phenomena observed in metamaterials.

**Results**

**Photonic analog to the Dirac equation.** A 1D plane electromagnetic wave of the frequency $\omega$ in an optical media can be described by Maxwell’s equations

$$-\partial_t E_z = i\omega \mu_0 \mu_r(x) H_z,$$

$$\partial_x H_y = -i\omega \varepsilon_0 \varepsilon_r(x) E_z.$$  

(1)

(2)

Here, $E_z$ and $H_y$ are the electric and magnetic fields, $\varepsilon_0$ and $\mu_0$ ($\varepsilon_r$ and $\mu_r$) are the vacuum (dimensionless relative) permittivity and permeability of the media, respectively, which can be functions of position in artificially designed optical materials. By introducing the spinor $\varphi = \left( \sqrt{\varepsilon_0} E_z \sqrt{\mu_0} H_y \right)$, Eqs. (1) and (2) can be written as,

$$[-i\sigma_z \partial_x + m(x) \sigma_z + V(x)] \varphi = E \varphi.$$  

(3)

Here $m(x) = \frac{\omega^2}{2c} [\varepsilon_r(x) - \mu_r(x)]$ and $V(x) = \frac{\omega^2}{2c} [\varepsilon_r(x) + \mu_r(x) - \langle \varepsilon_r(x) + \mu_r(x) \rangle]$ are the effective mass and potential, respectively, $E = -\frac{\omega^2}{2c} (\varepsilon_r(x) + \mu_r(x))$ is the energy eigenvalue, $c$ is the speed of light in vacuum, and $\sigma_1, \sigma_2, \sigma_3$ are the three Pauli matrices. Equation (3) is equivalent to the stationary Dirac equation in a potential $V(x)$ by taking the Planck constant $\hbar$ and $c$ as units. In this way we have established a one-to-one mapping between Maxwell’s equations and the Dirac equation, which provides a platform to study relevant problems of the Dirac equation in metamaterials with engineered permittivity and permeability.

It is noted that the effective mass in Eq. (3) is given by the permittivity and permeability, which can be tailored controllably by artificially designed structures in metamaterials. The signs of permittivity and permeability determine the chirality of electromagnetic wave in optical media: the electric field, magnetic field and the wave vector obey the right-handed or left-handed triad. For ordinary (nonmagnetic) optical materials $\varepsilon_r > \mu_r = 1$, the electromagnetic wave obeys the right-handed rule with a positive effective mass $m > 0$ while the double-negative or left-handed metamaterials with $\varepsilon_r < \mu_r < 0$ have a negative mass $m < 0$ and obey the left-handed rule. On the other hand, it is known that the sign change of the effective mass accompanying the band inversion is closely related to the topological order of a medium. Therefore, the present study is the first one, to the best of our knowledge, to illustrate the possible relation between topological order in condensed matters and chirality feature in metamaterials. We believe that this relation will open a new route to mimic topological phases and excitations of Dirac equation in designed metamaterials, and to understand some exotic phenomena in metamaterials from a point of view of the Dirac equation.

**Simulation of the band inversion in the Dirac equation.** The Dirac equation demands the existence of anti-particle, the particles with negative energy and negative mass. The solutions of positive and negative energy automatically satisfy the Einstein mass-energy relation as a consequence of special theory of relativity. To interpret the solutions, Dirac proposed that the negative energy solution is for a positron with negative mass, an anti-particle of electron. According to the Pauli exclusion principle, an electron cannot occupy the state of negative energy as all the states with negative energy are supposed to be fully filled. There exists an energy gap $2m_e c^2$ ($m_e$ is the rest mass of electrons) between the positive energy band for an electron and the negative energy band for positron. As the rest mass of electron is very huge, $m_e c^2 = 0.53$ MeV, a positron can only be observed in high energy physics. However, the mapping between Maxwell’s equations and the Dirac equation in 1D offers an alternative approach to realize the band inversion, i.e., the sign change of effective mass in the Dirac equation, because either the permittivity $\varepsilon_r$ or permeability $\mu_r$ in metamaterials can be manipulated in a controllable way.

Specifically, to bridge the photonic gap and the Dirac gap, we calculate the dispersion relation from the perspective of the Dirac equation as shown in Eq. (3). By treating metamaterials with subwavelength unit cell as an effective media with complex electric and magnetic responses, we can obtain the dispersion relation,

$$k^2 = (V - E)^2 - m^2 = \frac{\omega^2}{c^2} \varepsilon_r \mu_r.$$  

(4)

Here $k$ is real if $\varepsilon_r \mu_r > 0$, corresponding to either the positive-index band with right-handed chirality or negative-index band with left-handed chirality. In contrast, $k$ has a purely imaginary value if $\varepsilon_r \mu_r < 0$, which indicates the existence of a band gap. It follows from Eq. (3) that the gap can be characterized as either positive or negative mass.

Microwave experiments based on transmission-line (TL) metamaterials are performed to realize the band inversion from positive to negative mass. The TLs are all fabricated on copper-clad 1.57-mm thick Rogers RT5880 substrates, whose relative permittivity and tangent loss are $\varepsilon_r = 2.2$ and $\tan\delta = 0.0009$, respectively. Two 50 $\Omega$ subminiature version A (SMA) connectors are used as the input and output ports. The unit cell of this structure consists of a shunt inductance $L$ in parallel with a capacitance $C_0$ brought by the TL segment and a capacitance $C$ in series with an inductance $L_0$ attributed to the TL segment. A circuit model to describe electromagnetic response of the CRLH TL metamaterials was established in Refs. 26 and 27. The validity of the model has been studied extensively in metamaterials, and many novel phenomena based on CRLH TL metamaterials, such as negative refraction and super-resolving lens, are successfully described by the model as summarized in Refs. 28 and 29. It gives the effective permittivity and permeability of the CRLH TL in the long-wavelength limit as,

$$\tilde{\varepsilon}_r = \frac{1}{p\varepsilon_r} \left( C_0 - \frac{1}{\omega^2 L d} \right) + \frac{\gamma_2}{\omega}, \quad \tilde{\mu}_r = \frac{p}{\mu_r} \left( L_0 - \frac{1}{\omega^2 C d} \right) + \frac{\gamma_m}{\omega},$$  

where $\varepsilon_r$ and $\mu_r$ are the permittivity and permeability of environment media, respectively, $C_0$ ($L_0$) is the per-unit-length capacitance (inductance) of the TL segment, $C$ ($L$) is the series capacitance (the shunt inductance) of the loading elements, $\gamma_2$ and $\gamma_m$ denote the losses, $d$ is the length of a unit cell, and $p$ is the geometric factor. We would like to emphasize that these parameters can be tailored experimentally. For example, we can tune the frequency $\omega$ or the length of a unit cell $d$ to change the values of the permittivity and permeability continuously. The effective loss in a sample can be deduced from the experimental measurement of transmission and reflection of a sample. It is worthy stressing that the limitation of this model is that the size of each unit cell is required to be smaller than a quarter wavelength. In this experiment, the unit cell has a length of $d = 8\text{ mm}$ (which is less than 1/10 wavelength in the microstrip), and an electromagnetic wave does not “see” discontinuities of the structure. Thus the CRLH TL can be considered effectively homogenous. From the frequency-dependent $\tilde{\varepsilon}_r$ and $\tilde{\mu}_r$, the two band edges $\omega_1$ and $\omega_2$ are determined by setting $\tilde{\varepsilon}_r = 0$ or $\tilde{\mu}_r = 0$, respectively. For simplicity here, we assume $\gamma_2 = \gamma_m = 0$, and the band edges is obtained as

$$\omega_1 = \frac{1}{\sqrt{L_0 C d}}, \quad \omega_2 = \frac{1}{\sqrt{L C d}}.$$

(6)

The frequency difference between $\omega_1$ and $\omega_2$ defines the energy gap as shown in Fig. 1(a). The gap closing at $\omega_1 = \omega_2$ or $m = 0$ gives rise to the Dirac point, where some interesting behaviors have been reported, such as Zitterbewegung\(^{30}\), wave bending and cloaking.
effect\textsuperscript{41}. It is clear that the frequencies can be readily tuned by tailoring \( C_0, L_0, C, \) and \( L \). If we can adjust the band edges from \( \omega_1 < \omega_2 \) to \( \omega_1 > \omega_2 \) or vice versa, the band inversion would be achieved.

The band inversion is illustrated in the simulated and measured density of states (DOS) in Fig. 1. Note that both \( C_0 \) and \( L_0 \) are functions of the width of the TL, \( w \). With an increase of \( w, C_0 \) increases, but \( L_0 \) decreases. Consequently, one band edge moves to a higher frequency, while the other moves to a lower frequency. Therefore in a well-designed structure, the band inversion is expected to occur by adjusting the width \( w \). We designed several samples and calculated their width-dependent dispersions, and observed the band inversion illustrated in Fig. 1(a). It is noted that the band structure inversion accompanies an change of the band edges, and the effective mass also changes its sign. This feature is closely related to the chirality of electromagnetic wave in the designed sample as shown in Fig. 1(b).

Before band inversion, the edge of \( \mu = 0 \) locates at higher frequency and connects to the pass band with right-handed chirality for \( \nu_r > \mu_r > 0 \) while the edge of \( \nu_r = 0 \) locates at lower frequency and connects to the pass band with left-handed chirality for \( \mu_r < \nu_r < 0 \), as shown in Fig. 1(b.i). After band inversion from \( m > 0 \) to \( m < 0 \), the two band edges are exchanged with each other as shown in Fig. 1(b.ii): the edge of \( \mu_r = 0 \), for example, moves to the lower frequency and connects to the pass band with left-handed chirality for \( \nu_r < \mu_r < 0 \). The physical picture of the band inversion can be understood as an electromagnetic state \((E, H)\) moving from \((\omega_0 + \Delta \omega, k)\) to \((\omega_0 - \Delta \omega, -k)\) in the dispersion relation, where \( \omega_0 \) is the frequency of the Dirac point. It is characterized by the sign change of effective mass accompanied by the conversion of electromagnetic chirality. Now it is already known that the sign of the mass in Dirac equation can be used to describe different topological order in condensed matters\textsuperscript{23,24}. Therefore, the above picture shows us a clear connection between topological order in condensed matter systems and chirality in metamaterials: when the chirality of a band changes, its topological order changes.

To illustrate the band structure experimentally we fabricated a series of samples with different widths and measured the DOS for microwaves. Each sample contains 24 units, and each unit has a length of \( d = 8.5 \text{ mm} \) with a series capacitor \( C = 3.3 \text{ pF} \) and a shunt inductor \( L = 10 \text{ nH} \). Agilent PNA Network Analyzer N5222A was employed to measure the reflection, transmission, and group delay of the samples. The DOS of a lossless optical system is proportional to the group delay \( \tau_g(\omega) = \frac{1}{\pi} \frac{d}{d\omega} \frac{\tau_g}{\tau_g(D)} \) (where \( D \) is the total length of the sample)\textsuperscript{32}. In practice, dissipation is inevitable in the transmission line experiments, and the wave vector \( k \) is no longer purely real and the DOS is not well defined. However the group delay is still measurable. When the imaginary part of the effective mass in Eq. (3) is comparably small, it is a good approximation to define DOS by using the group delay. Meanwhile we also calculated the DOS with a fitted loss from experimental data. The numerical and experimental results are presented in Figs. 1(c) and 1(d), respectively. It is clearly shown that the band gap gradually closes up as \( w \) decreases to a critical point of \( w_0 \approx 4.5 \text{ mm} \). With a further decrease of \( w \), a gap re-opens again. It is worth pointing out that the loss is introduced in the effective permittivity and permeability while the numerical simulation is performed. The values of \( \gamma_r \) and \( \gamma_i \) are taken to be 0.24 by fitting the experimental data. For comparison we also present the result (see the solid line in Fig. 1c) without the loss, the discrepancies between the two cases are very clear. Considering the loss in the sample, the measured data are in a good agreement with the calculated results. In this way we have successfully demonstrated the band inversion in the metamaterials experimentally. This provides an explicit and solid foundation for photonic simulation of the Dirac equation in metamaterials.

**Soliton solution for a domain wall.** The Jackiw-Rebbi solution describes the bound state of a particle to the interface or domain wall between two media with positive and negative masses\textsuperscript{32}. For simplicity consider two 1D media with positive mass \( m_1 > 0 \) and negative mass \( -m_2 < 0 \) forming a domain wall at \( x = 0 \) with a potential \( V(x) = 0 \). It is found that there exists an analytical solution of zero energy \( (E = 0) \),

\[
\psi(x) = \sqrt{\frac{m_1 m_2}{m_1 + m_2}} \left( 1 - it \right) \exp[-im(x)x],
\]

which decays exponentially in \( |x| \). It is a solution of 1D topological excitation or soliton, which is robust even for irregular distribution of mass near the interface, and has potential application. For example, the charge carriers in 1D organic conductors are attributed to the solitons and anti-soliton\textsuperscript{34,35}. However, it is still an experimental challenge to observe a single soliton in a 1D polymer due to small lattice spacing\textsuperscript{36,37}. Simulation of the model was also proposed to realize in other systems, such as an atomic Dirac-Fermi gas on an optical lattice\textsuperscript{38}. In metamaterials, a solution for a resonant mode at an interface between two slabs of epsilon-negative and mu-negative media was obtained by solving Maxwell’s equations explicitly\textsuperscript{39} and also confirmed experimentally\textsuperscript{40,41}. However, its topological origin was not recognized so far.

Here we demonstrate that the Jackiw-Rebbi solution can be realized in the metamaterials by constructing a domain wall with controllable parameters. To this end, we fabricated a sample consisting of two TL metamaterials, \( w_1 = 2.5 \text{ mm} \) and \( w_2 = 8.5 \text{ mm} \). Both metamaterials have finite gaps, but with opposite masses as illustrated in Figs. 1(c) and 1(d). However, when these two TL metamaterials are connected, it is found that an additional narrow peak appears at \( \omega_0 = 11.05 \text{ GHz} \) within the gap region in the DOS as shown in Fig. 2(a). The parameters at \( \omega_0 = 11.05 \text{ GHz} \) are given by \( m_1 = -11.83, V_1 = 0.26 + 0.80i, m_2 = 16.65, \) and \( V_2 = -0.26 + 0.80i \). The corresponding energy of the resonant peak is \( E = 0.03 \), whose nonzero value is caused by the energy loss or the imaginary part of the potential. Figure 2(b) shows the full-wave simulation of field spatial distribution in the sample at \( \omega_0 \) which was obtained by using a commercial software package (CST Microwave Studio). It is clearly seen that the incident field increases to reach a maximal, and then decays exponentially, indicating a well-defined bound state.

We also carried out microwave experiments in time domain to investigate the field distribution. The result is presented in Fig. 2(c), which is in good agreement with the numerical simulation. Note that in each unit cell, only one position near the shunt inductor is probed, and thus the LC resonances within a unit are not detected. The measured peak of the incident field is attributed to the non-linear or topological excitation described by Jackiw-Rebbi solution. Thus this measurement provides the direct observation of the Jackiw-Rebbi solution or the profile of soliton in a photonic simulator made of metamaterials.

**Simulation of a 1D lattice topological phase.** The metamaterials with different effective masses provide building blocks to construct various artificial optical materials to simulate solid state systems. In condensed matter, the simplest “two-band” model is the Su-Schrieffer-Heeger model for polyacetylene\textsuperscript{39}. Consider a 1D dimerized lattice with bipartite lattice sites A and B. Each unit cell consists of two sites A and B. The hopping amplitude between two sites in a unit cell is \( t + \delta t \) and that between two unit cells is \( t - \delta t \).

When \( \delta t = 0 \), the energy dispersion presents \( E = \pm 2t \cos \frac{k}{2} \). For half filling, due to the Peierls’ instability, the dimerization occurs and \( \delta t \neq 0 \); an energy gap opens, and is equal to \( 4t \delta t \). According to the sign of \( \delta t \), the gap can be either positive or negative. The inverted band structure is closely related to topological insulators, such as Bi\(_2\)Te\(_3\) and Bi\(_2\)Se\(_3\). The topological property of this 1D model can be also determined by the Berry phase of the lower energy band, which is given by \( \pi (\text{sgn} (t + \delta t) \times \text{Re} \theta ) \) where \( \theta \) is the Berry phase of the lower energy band.

\( \theta \) is the Berry phase of the lower energy band, which is given by \( \pi (\text{sgn} (t + \delta t) \times \text{Re} \theta ) \) where \( \theta \) is the Berry phase of the lower energy band.
The difference of the Berry phases for $\delta t > 0$ and $\delta t < 0$ is $\pi$, which indicates that the two phases are topologically distinguished: one is topologically trivial and the other one is topological non-trivial. The topologically non-trivial phase is characterized by the presence of end state of zero energy in an open boundary condition\textsuperscript{44,45}. Though it is believed that the end states should exist in 1D polymer, it is a great challenge for experimentals to measure them experimentally.

To mimic such topological phases in a lattice structure, we design a periodic stack of two TL blocks with $m_A > 0$ (w = 7 mm) and $m_B < 0$ (w = 4 mm), as shown in Figs. 3 and 4(a). The unit of the samples has a length of $d = 7$ mm with a series capacitor $C = 1.0$ pF and a shunt inductor $L = 3.3$ nH, leading to $|m_A| > |m_B|$. This periodic structure can be used to simulate the Su-Schrieffer-Heeger model. Different $m_A > 0$ and $m_B < 0$ corresponds to the positive and negative $\delta t$. In the periodic boundary condition, the theoretical calculation shows that dispersion relation have the similar band structure of the Su-Schrieffer-Heeger model, which exhibits the presence of an energy gap $\delta \omega = 1.46$ GHz between two band edges at $\omega_1 = 13.53$ GHz and $\omega_2 = 14.99$ GHz, as shown in Fig. 4(b).
distribution of the end mode corresponding to (d). (f) Measured voltage as the field distribution in the sample.

In the present experiment, we fabricated two structures by removing one block of the ideal periodic structure. A band gap of \( \delta \omega = 1.46 \) GHz is present between \( \omega_1 = 13.53 \) GHz and \( \omega_2 = 14.99 \) GHz. (c) The measured DOS for the structure lacking of a mass \( m_1 \) component. Two band edges appear at \( \omega_1 = 13.31 \) GHz and \( \omega_2 = 15.23 \) GHz, whose value is close to the calculated value of the loop. The non-zero DOS is attributed to the loss of the metamaterials, which is characterized by the parameters \( \gamma_c \) and \( \gamma_m \) in Eq. (5). They are fitted to be 0.24 from the measured data. The second case in Fig. 4(c) exhibits a similar band structure as in Fig. 4(c), but presents an additional peak at \( \omega_0 = 14.18 \) GHz between the two peaks at \( \omega_1 = 12.73 \) GHz and \( \omega_2 = 16.10 \) GHz. A more detailed analysis indicates that the two peaks at \( \omega_1 = 12.73 \) GHz and \( \omega_2 = 16.10 \) GHz correspond to the band edges as shown in Fig. 4(b), in which slight shifts of the position are caused by the finite size effect. The resonant peak at \( \omega_0 = 14.18 \) GHz corresponds to two bound states at the ends, which can be seen clearly in Figs. 4(e) and 4(f). This indicates that the topological properties of the two designed chains are topologically distinguished, although they are constructed by the same blocks of \( w = 7 \) mm and \( w = 4 \) mm. Thus our measurements demonstrate explicitly the existence of the end states in 1D topological systems.

**Discussion**

In summary, we have demonstrated an explicit mapping between Maxwell’s equations and the Dirac equation in one dimension. This provides a platform to utilize the electromagnetic wave to mimic quantum phenomena related to the Dirac equation from high-energy physics to condensed matter physics. In the form of the Dirac equation, the effective mass is determined by the permittivity and permeability of the media. While the absolute sign of mass has no special physical meaning, the sign change of the mass is closely related to the topological order of a medium. We can make use of this property to...
generate photonic counterparts of 1D topological excitations. By tailoring the permittivity and permeability of metamaterials, band inversion of the Dirac equation was demonstrated theoretically and experimentally. It has been found that the band inversion accompanies a change of chirality of electromagnetic wave in metamaterials. Furthermore, we have designed and fabricated transmission-line structures to demonstrate some important solutions of the Dirac equation, such as soliton solution for a domain wall and the Su-Schrieffer-Heeger model for polyacetylene. Different from the previous topological excitations in two-dimensional photonic lattice structures where an effective Dirac equation was derived near the Dirac point in a long wave limit, we write the 1D Maxwell’s equations explicitly in the form of Dirac equation and propose to stimulate topological excitations by engineering the electromagnetic responses of metamaterials. Our numerical simulation and microwave experiments illustrated a proof-of-principle example that metamaterials are ideal candidates to simulate topological phenomena in solids, and the behaviors of the Dirac equation.

Methods

The TLs are all fabricated on copper-clad 1.57-mm thick Rogers RT5880 substrates. A network analyzer (Agilent PNA N5222A) was used to characterize our samples in the Supplementary Information. It has been found that the band inversion accompanies a change of chirality of electromagnetic wave in metamaterials. Furthermore, we have designed and fabricated transmission-line structures to demonstrate some important solutions of the Dirac equation, such as soliton solution for a domain wall and the Su-Schrieffer-Heeger model for polyacetylene. Different from the previous topological excitations in two-dimensional photonic lattice structures where an effective Dirac equation was derived near the Dirac point in a long wave limit, we write the 1D Maxwell’s equations explicitly in the form of Dirac equation and propose to stimulate topological excitations by engineering the electromagnetic responses of metamaterials. Our numerical simulation and microwave experiments illustrated a proof-of-principle example that metamaterials are ideal candidates to simulate topological phenomena in solids, and the behaviors of the Dirac equation.
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