This is the accepted manuscript made available via CHORUS. The article has been published as:

Excitonic effects in the optical properties of a SiC sheet and nanotubes
H. C. Hsueh, G. Y. Guo, and Steven G. Louie
Phys. Rev. B 84, 085404 — Published 19 August 2011
DOI: 10.1103/PhysRevB.84.085404
Excitonic effects in the optical properties of SiC sheet and nanotubes

H. C. Hsueh,1,* G. Y. Guo,2,3,† and Steven G. Louie4,5

1Department of Physics, Tamkang University, Tamsui, Taiwan 25137, Taiwan
2Graduate Institute of Applied Physics, National Chengchi University, Taipei 11605, Taiwan
3Department of Physics, National Taiwan University, Taipei 10617, Taiwan
4Department of Physics, University of California at Berkeley, Berkeley, California 94720, USA
5Materials Sciences Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA

The quasiparticle band structure and optical properties of single-walled zigzag and armchair SiC nanotubes (SiC-NTs) as well as single SiC sheet are investigated by \textit{ab initio} many-body calculations using the GW and the GW plus Bethe-Salpeter equation (GW+BSE) approaches, respectively. Significant GW quasiparticle corrections of more than 1.0 eV to the Kohn-Sham band gaps from the local density approximation (LDA) calculations are found. The GW self-energy corrections transform the SiC sheet from a indirect LDA band gap to a direct band gap material. Furthermore, the quasiparticle band gaps of SiC-NTs with different chiralities behave very differently as a function of tube diameter, and this can be attributed to the difference in the curvature-induced orbital rehybridization between the different chiral nanotubes. The calculated optical absorption spectra are dominated by discrete exciton peaks due to exciton states with large binding energy up to 2.0 eV in the SiC sheet and SiC-NTs. The formation of strongly bound excitons is attributed to the enhanced electron-hole interaction in these low dimensional systems. Remarkably, the excited electron amplitude of the exciton wavefunction is found to peak on the Si atoms near the hole position (which is on the C site) in the zigzag SiC-NTs, indicating a charge transfer from an anion (hole) to its neighboring cations by photoexcitation. In contrast, this pronounced peak structure disappear in the exciton wavefunction in the armchair SiC-NTs. Furthermore, in the armchair SiC-NTs, the bound exciton wavefunctions are more localized and also strongly cylindrically asymmetric. The large excitation energy of \(\sim 3.0\) eV of the first bright exciton with no dark exciton below it, suggests that the small-radius armchair SiC-NTs be useful for optical devices working in the UV regime. On the other hand, the zigzag SiC-NTs have many dark excitons below the first bright exciton and hence may have potential applications in tunable optoelectric devices ranging from infrared to UV frequencies by external perturbations.

PACS numbers: 81.07. De, 73.22.-f, 78.67.Ch, 73.63.Fg

INTRODUCTION

Silicon carbide (SiC) crystallizes in either a cubic or a hexagonal form, and exhibits interesting polytypism [1, 2]. The polytypes are made of identical hexagonal layers with different stacking sequences. These polytypes are semiconductors with a range of band gaps, from 2.39 eV in the zincblende polytype (3C) to 3.33 eV in the wurtzite polytype (2H) [1, 3]. Furthermore, 3C and 6H SiC are used for high temperature, high-power and high-frequency devices [4–7] due to their unique properties [8], while 6H SiC with a band gap of 2.86 eV is a useful material for blue light-emitting diode applications [3].

Recently, SiC nanotubes (NTs) were synthesized by reaction of carbon nanotubes (CNTs) with SiO at various temperatures [9]. Like other tubular materials such as C [10–12], BN [13, 14], AlN [15], and GaN [16] nanotubes that have been synthesized previously, SiC-NTs display very interesting properties distinctly different from their bulks. Therefore, the successful synthesis of the SiC-NTs has stimulated a number of theoretical and experimental investigations on tubular form of SiC (see [17, 18] and references therein). In particular, based on density-functional calculations, Miyamoto and Yu [19] predicted that the strain energies of SiC-NTs are lower than that of CNTs, and that the band gaps of SiC-NTs can be direct or indirect, depending on the chirality. Using both tight-binding molecular dynamics and \textit{ab initio} methods, Menon and coworkers [20] showed that single-walled SiC-NTs are very stable with a large band gap.

Unlike CNTs, SiC-NTs are polar materials and therefore, may exhibit unusual physical properties that CNTs may not have. For example, like BN-NTs (see, e.g., [21, 22]), zigzag SiC-NTs may become piezoelectric, and also show second-order non-linear optical response. A knowledge of the optical properties of SiC-NTs is important for their optical and electro-optical applications. Therefore, Wu and Guo have recently carried out a series of \textit{ab initio} calculations within the density functional theory (DFT) with the local density approximation (LDA) in order to analyze the linear optical features and underlying band structure as well as the second-harmonic generation and linear electro-optical coefficients of all three types of the SiC-NTs.[17, 18] In particular, Wu and Guo found that all the SiC nanotubes are semiconductors with exceptions of the ultrasmall (3,0) and (4,0) zigzag tubes which may be regarded as the thinnest conducting SiC nanowires.[17] Interestingly, the band gap of the zigzag SiC-NTs may be reduced from the energy gap of the SiC sheet all the way down to zero by reducing the diameter,
though the band gap for all the SiC nanotubes with a diameter larger than $\sim 20$ Å approaches that of the SiC sheet. Furthermore, DFT indicates that all the semiconducting zigzag SiC-NTs have a direct band gap. All these suggest that they may have interesting applications in optical and optoelectronic devices. Nonetheless, both the armchair and chiral SiC-NTs have an indirect band gap at the DFT level.

These previous theoretical studies of the electronic and optical properties of SiC-NTs were based on the independent-particle approximation within the DFT framework[17, 18] or on semi-empirical calculations[20]. However, many-body interactions are known to play an important role in low-dimensional systems such as nanotubes[23, 24], due to reduced charge screening and enhanced electron-electron correlation. Therefore, motivated by the prospects of optoelectronic device applications of SiC-NTs and also this theoretical issue, we have performed ab initio calculations to study the many-body effects on the quasiparticle band gaps and optical spectra of SiC-NTs. Indeed, we find pronounced GW quasiparticle corrections of more than 1.0 eV to the LDA band gaps in the SiC-NTs. Further, the calculated optical absorption spectra from the SiC-NTs are dominated by the discrete exciton peaks due to strongly bound excitons with a large binding energy of up to 2.0 eV.

SiC-NTs can be considered as an atomic layer of SiC sheet rolled up into a cylinder, and similar to the CNTs the structure of a SiC-NT is specified by the chiral vector which is given in term of a pair of integers $(n, m)$.[11] Understanding the optical properties of an isolated SiC sheet would help understand the many-body effects on the optical responses of SiC-NTs. Therefore, the single atomic layer hexagonal SiC sheet is first considered here. Furthermore, the optical properties of the two-dimensional (2D) single SiC sheet are interesting on their own account, and, in particular, a single SiC sheet bears many similarities to graphene which exhibits many fascinating properties.[25, 26]

This paper is organized as follows. In the next section, the theoretical methods and computational details, including the ground-state, quasiparticle and electron-hole interaction calculations, are described. In Sec. III, the calculated quasiparticle band structure and optical absorption spectrum of the isolated SiC sheet are presented. In Sec. IV, the calculated quasiparticle band structures of the SiC-NTs are reported and the effects of curvature and chirality on the band gaps are analyzed. In Sec. V, the calculated optical absorption spectra of the SiC-NTs are presented, and the excitonic effects are discussed. Finally, the conclusions drawn from this work are given in Sec. VI.

**METHODOLOGY**

In the present paper, we adopt the approach of Rohlfing and Louie[27, 28] and hence calculate the quasiparticle energies, electron-hole excitations and optical spectra from first-principles in three steps. First, we calculate the electronic ground state with DFT in the LDA.[29] Second, we obtain the quasiparticle energies ($E^{QP}$) within the GW approximation for the electron self energy $\Sigma$.[30, 31] Finally, we evaluate the coupled electron-hole excitation energies and optical spectra by solving the Bethe-Salpeter equation (BSE) of the two-particle Green’s function.[27, 28] Details of our computations are described below.

**Ground-state properties**

An appropriate mean-field description of the ground-state properties of solids is essential to perform quasiparticle calculations within many-body perturbation theory. For the conventional covalent and ionic bonded materials, it is shown [31] that eigen wavefunctions and eigen energies of the Kohn-Sham equation in the LDA provide a good starting point for the many-body perturbation calculations such as within the GW approximations. Therefore, in this paper, the ground-state electronic structure of the single SiC sheet and SiC-NTs are first calculated by means of ab initio plane-wave pseudopotential method[32]. The electronic configurations of Si$(3s^2, 3p^2)$ and C$(2s^2, 2p^2)$ are treated as active valence states when generating pseudopotentials in the Kleinman-Bylander form[33] for all the calculations. The cutoff energy of 40 Ry for the plane wave basis set is used. Also to ensure the convergency, the Brillouin zone (BZ) integrals for the calculations of the SiC sheet and SiC-NTs are carried out using the $10 \times 10 \times 1$ and $1 \times 1 \times 32$ Monkhorst-Pack $k$-grid sampling[34], respectively. The supercell approach is used here such that an isolated SiC sheet (nanotube) is approximated by a single SiC layer (nanotube) surrounded by vacuum in a supercell. Sufficient intersheet and intertube separations (more than 10 Å) are used to prevent intersheet and intertube interactions. The underlying atomic positions and lattice constants are taken from Ref. [17] where the theoretical structures were obtained by the conjugate gradient method with the atomic forces and the stress calculated from first-principles.

**Quasiparticle calculations**

Based on the ground-state Kohn-Sham wavefunctions and corresponding eigenvalues ($E^{KS}$) calculated above, the many-body effects on the quasiparticle band structure characterized by the self energy ($\Sigma$) can be evaluated.
The electronic excitation and even transport properties of a solid plays an important role in obtaining reliably its quasiparticle properties. In low dimensional systems, such requirement becomes crucial due to the highly anisotropic screening interactions associated mainly with the vacuum region between the isolated units in the supercell scheme. A larger vacuum region is preferred to reduce the residual unphysical inter-unit interaction and eventually ends up with an ideal vacuum screening of the isolated units. For example, the band gap of an isolated SiC sheet, as shown in Fig. 1, would increase as the screening from neighboring layers is reduced by increasing the separation ($L_z$) between the SiC layers in the neighboring supercells. Furthermore, the convergence of the band gap with respect to the spatial separation of the neighboring SiC layers is very slow. Due to the computation constraints, it is impossible to obtain the fully converged band gap simply by expanding the inter-layer separation. Therefore, an efficient truncation scheme[39, 40] to the Coulomb interaction in which a step function at the boundary of the supercell is introduced, will be adopted in the present GW and BSE calculations to remove the long-range Coulomb interaction between the structure and its images. Fig. 1 clearly demonstrates that the truncation scheme indeed offers an efficient means to achieve the converged quasiparticle band gap for the low-dimensional structures. Table I further shows that the quasiparticle band gap and also quasiparticle energy differences from the GW calculations with or without the Coulomb truncation scheme can differ significantly.

### Electron-hole excitations

The optical properties of a solid, associated with the interaction between light and the electronic excitations of a system, are described by the frequency-dependent macroscopic dielectric function $\epsilon(\omega)$. For example, the optical absorption spectrum is determined by the imaginary part of the dielectric function, $\epsilon_2(\omega)$. According to

![Graph showing calculated quasiparticle band gap as a function of the inverse of intersheet separation ($L_z$).](image)

**FIG. 1.** The calculated quasiparticle band gap of a SiC sheet (open symbols) as a function of the inverse of intersheet separation ($L_z$). The converged band gap indicated as the solid line is derived by employing the Coulomb truncation scheme. The dashed line linking the open circles is a guide to the eye only.

by solving the Dyson equation [30, 31, 35]

$$
H_0 + \Sigma(E_{nk}^{QP}) |n\k\rangle = E_{nk}^{QP} |n\k\rangle
$$

where $H_0$ is the Hamiltonian in the Hatree approximation, and $|n\k\rangle$ represents the quasiparticle wavefunction of energy $E_{nk}^{QP}$ within one-particle Green’s function method. In the $G^0W^0$ approximation, the vertex correction is approximated by a delta function and the irreducible polarizibility $P^0$ is a convolution of the mean field Green’s function $G^0$, i.e., $P^0 = -iG^0 G^0$. This gives rise to a dynamical dielectric matrix within the random phase approximation (RPA) scheme and a generalized plasmon-pole (GPP) model[31]. Also, the screened Coulomb potential $W^0$ can be obtained from the bare Coulomb interaction $v$ through the equation $W^0 = v/[1 - vP^0]$. Finally, the quasiparticle self-energy operator is given by $\Sigma = iG^0W^0$. Although alternatives have been proposed recently to calculate the self energy going beyond this approximation, the $G^0W^0$ approach is still the most efficient scheme for providing a successful description of the electronic excitation and even transport properties in various semiconductors, metals, surfaces, and novel nanomaterials[36–38]. Therefore, in this paper, we adopt the $G^0W^0$ approach to calculate the quasiparticle properties of the single SiC sheet and SiC-NTs. Here a rather dense $k$-point sampling for the SiC sheet (18×18×1) and also for the SiC-NTs (1×1×32) is used to ensure the calculated quasiparticle energies converged to within 0.05 eV.

A proper description of the dynamical screening prop-

### Table I. The band gap ($E_{gap}$) and quasiparticle energy differences between the conduction band minimum ($c$) and valence band maximum ($v$) at some high symmetry $k$-points of the SiC sheet from the LDA and GW [without/with the Coulomb truncation (no trunc.)/(trunc.)] calculations. All energies are in eV.

|          | LDA      | GW (no trunc.) | GW (trunc.) |
|----------|----------|----------------|-------------|
| $E_{gap}$ | 2.51     | 3.66           | 4.42        |
| $K^v \rightarrow K^c$ | 2.56 | 3.66           | 4.42        |
| $\Gamma^v \rightarrow \Gamma^c$ | 4.46 | 5.58           | 6.04        |
| $M^v \rightarrow M^c$ | 3.23 | 4.60           | 5.40        |
the Fermi Golden rule, the transition energy associated with a peak in the optical absorption spectrum can be estimated from the energy difference between the associated electron and hole states. The corresponding oscillator strength can be obtained from the optical transition matrix elements derived from the electronic ground and excited states involved. Since the incident photons carry negligible momentum, the peaks in the optical absorption spectrum can be considered as direct interband transitions between the occupied and unoccupied electronic states without any crystal momentum transfer. Therefore, if ignoring the electron-hole interaction, both linear and nonlinear optical spectra can be calculated in an independent-particle approximation by including only the vertical interband transitions between the Kohn-Sham states[17, 18]. In the GW+RPA approach, the dielectric function calculated based on the quasiparticle energies as described above, gives the interband optical absorption spectrum beyond the LDA, but still without electron-hole interaction (or excitonic) effects.

However, for the systems with strong excitonic effects, the optical properties may be dominated by excitons which are composed of strongly correlated electron-hole pairs of the systems. The connection of the exciton energies $\Omega^S$ and corresponding electron-hole amplitudes $A_{vck}^S$ of the correlated electron-hole excitations $S$ is governed by the Bethe-Salpeter equation[28]

$$(E_{ck} - E_{ck}) A_{vck}^S + \sum_{v'c'k'} <vck|K^{ph}|v'c'k'> A_{v'c'k'}^S = \Omega^S A_{vck}^S$$

(2)

where $E_{ck}(E_{ck})$ denotes the quasiparticle (e.g., GW) eigenvalues of valence (conduction) bands at a specific $k$-point and $K^{ph}$ is the kernel describing the interaction between excited electrons and holes. Therefore, a more realistic two-particle picture of the optical excitations including excitonic effects in these systems should be provided by means of the GW+BSE method. To obtain the converged optical spectra, in the present work, the kernel $K^{eh}$ of the SiC sheet (SiC-NTs) is computed on a sparse $k$-point grid of $18 \times 18 \times 1$ ($1 \times 1 \times 32$) and then interpolated[27] onto a denser $k$-point grid of $36 \times 36 \times 1$ ($1 \times 1 \times 64$).

Instructively, the electron-hole amplitude in real space can be expanded in the quasi-electron and quasi-hole basis \{$\phi_{ek}(r_e), \phi_{hk}(r_h)$\},

$$\Phi_S(r_e, r_h) = \sum_k \sum_{v,c} A_{vcek}^S \phi_{ek}(r_e) \phi_{hk}(r_h)$$

(3)

and the corresponding exciton states can be visualized in real space. Because of the complexity of the six-dimensional exciton wavefunction, a simpler distribution of the electron amplitude square with the hole position fixed, i.e., $|\Phi_S(r_e, r_h = 0)|^2$, is usually used to reveal the essence of the electron-hole correlation of the exciton.[23, 24]

Finally, as noticed before[12, 17], the employment of a 3D supercell method for reduced-dimensional systems will generate an arbitrary volume effect on the dielectric function computation. In order to resolve this ambiguity and compare directly to experimental measurements, we calculate the imaginary part of polarizability per unit area (in units of nm) for the SiC sheet, \(\alpha_2(\omega)\), which is derived from the calculated dielectric susceptibility, \(\chi = (e - 1)/4\pi\), multiplied by the distance between two neighboring SiC sheets.[41] Moreover, for the one-dimensional (1D) nanotubes, the measured optical spectrum is determined by the imaginary part of the optical polarizability per single tube, \(\alpha_2(\omega)\). This \(\alpha_2\) is equal to the \(\epsilon_2^{calc}\) multiplied by the cross-sectional area of the supercell perpendicular to the tubular axis (\(\Lambda^{+}_{sc}\)), i.e., \(\alpha_2 = \Lambda^{+}_{sc} (\epsilon_2^{calc}) / 4\pi\).

**ELECTRONIC AND OPTICAL PROPERTIES OF SiC SHEET**

In the recent DFT-LDA calculations, a stable non-buckled graphene-like monolayer has been found for the isolated SiC layer[17, 42]. Despite the structural similarity, the unique massless Dirac fermion feature in graphene is no longer present in the SiC sheet because of the different ionicities of the Si and C atoms. This heteropolarity character induces an energy gap of 2.56 eV (the LDA value) at the $K$ point of the hexagonal Brillouin zone, as shown in Fig. 2. The quasiparticle corrections to the 2D SiC sheet state are obtained through the GW calculations described above. The calculated quasiparticle band gaps and energy differences at some high symmetry $k$-points are summarized in Table I. It is clear from Table I that the GW corrections to the LDA eigenvalues are rather significant, being more than 1.0 eV. We note that the GW correction to the LDA band gap of bulk 2H SiC is around 1.0 eV.[43, 44] Strikingly, the GW corrections transform the indirect LDA band gap ($K \rightarrow M$) into a direct band gap ($K \rightarrow K$) for the SiC sheet. The nature of the direct band gap in the 2D SiC sheet indicate that the lowest energy exciton in the SiC sheet is optically active (bright). Furthermore, based on the simple zone-folding approximation, we could expect no momentum-mismatch induced optically inactive (dark) excitons below the lowest energy bright exciton in the SiC-NTs[45]. This anticipation is indeed confirmed by our GW+BSE calculations for both the SiC sheet and armchair SiC-NTs presented below. However, our GW+BSE calculations also show that this is not the case for very small zigzag SiC-NTs, as will be discussed in Sec. V.

Figure 2 shows the LDA band structure (left panel) and also GW corrections to the LDA eigenvalues (right panel) of the 2D SiC sheet. We note that the optical dielectric function of the 2D SiC sheet is highly anisotropic.
fore, many-body interaction effects in the energy range (see Fig. 1 in Ref. 17). There-
amical screening for the in-plane electric field is strong in the sheet in the energy range below 6 eV, whereas the dy-
squares. The LDA
GW corrections of the NFE states are represented by green
line in Fig. 2) associated with the
p
bands (left panel) are denoted as red and blue lines, respectively. In the right panel, the GW corrections for the π and σ bands are represented by red circles and blue diamonds, respectively, whereas the GW corrections of the NFE states are represented by green
π
and
π∗
denoted as red and blue lines, respectively. In the right panel,
π−π∗
eigenvalues (\(E^{\pi-\pi^*}_{QP}\)) (red circles in Fig. 2). On the
σ−σ∗
eigenvalues (\(E^{\sigma-\sigma^*}_{QP}\)) (blue circles in Fig. 2). On the

FIG. 2. (Color online) The LDA band structure (left panel) and GW corrections to the LDA eigenvalues (right panel) of the graphitic SiC sheet. The π and σ bands (left panel) are represented by red circles and blue diamonds, respectively, whereas the GW corrections of the NFE states are represented by green squares. The LDA \(E^{\pi-\pi^*}\) gap is marked as an arrow in the left panel. The valence band maximum is aligned at 0 eV.

results with the GW+BSE calculations. Because of the huge depolarization effect in the 2-D planar geometry for light polarization perpendicular to the plane, we will focus on the optical absorption spectrum for light polarization parallel to the plane. Figure 3 shows the optical spectra from both the GW+RPA and GW+BSE calculations (a) as well as the \(E^{\pi-\pi^*}_{1}\) exciton wavefunction (b) of the SiC sheet. In Fig. 3(a), the first prominent peak located at \(E^{\pi-\pi^*}_{1} = 3.25\ eV\) in the GW+BSE absorption spectrum comes from a bright exciton due to the excitation between the π and π* states at the K point [see Fig. 2 (left panel)]. This is a strongly bound exciton with a large binding energy of \(E^{\pi-\pi^*}_{1} = 1.17\ eV\) as measured by the difference between the \(E^{\pi-\pi^*}_{1}\) and the onset energy of the GW corrected electron-hole continuum (\(E^{\pi-\pi^*} = 4.42\ eV\)). We note that the theoretical exciton binding energy in bulk 2H SiC is only 0.1 eV.[44] This shows clearly that the reduced dimensionality of a SiC sheet strongly confines the quasiparticles, and this significantly enhance the overlap between the electron and hole wave functions and hence the electron-hole interaction.

In addition to this quantum confinement, the presence of the vacuum region reduces the screening and hence provides extra contribution to the large excitonic effect in the SiC sheet. The analysis of \(\int |\Phi_S(r_e, r_h)|^2 dr_e\) and \(\int |\Phi_S(r_e, r_h)|^2 dr_h\) shows that the hole is mainly residing in the C-sublattice whereas the excited electron is on the Si-sublattice. In order to elucidate the extent of the \(E^{\pi-\pi^*}_{1}\) exciton wavefunction, we plot the electron amplitude square with the hole position fixed at the position slightly above the C atom (see Fig. 3b). Clearly, the electron orbital is of the \(p_z\) character, and distributes mainly on the nearest neighbor Si atoms around the hole to form a fairly localized exciton.

In the optical absorption spectrum of the SiC sheet \(\alpha_2(\omega)\) from the GW+BSE calculations, the low-energy features in the energy range from 3.0 to 5.0 eV (Fig. 3a) are dominated by the π → π* transitions near the K point at the zone edge (Fig. 2), whereas the pronounced absorption peak at 5.83 eV is mainly due to the σ → σ* transition at the zone center. As shown in Fig. 3(a), the electron-hole interaction not only triggers a red-shift of the onset optical transition energies but also modifies their relative absorption intensities. Furthermore, because the GW corrections transform the indirect LDA band gap of the SiC sheet into the direct band gap, as mentioned above, no dark exciton was found in the optical spectrum until the photon energy up to 4.2 eV which is above the lowest bright exciton (\(E^{\pi-\pi^*}_{1}\)).

QUASIPARTICLE BAND STRUCTURE OF SiC NANOTUBES

An intuitive approach to construct a nanotube with a specific chirality is simply to roll up a layer of the
FIG. 3. (Color online) (a) The optical polarizability per unit area from both GW+RPA (blue) and GW+BSE (red) calculations and (b) the $E^\pi_{1-\pi^*}$ exciton wavefunction of the SiC sheet. In (a), the theoretical spectra are broadened with a Gaussian smearing width of 0.15 eV. In (b), the hole position (red sphere) is fixed at the top of a C atom (yellow sphere) and the squared electron amplitude ($n = |\Phi_S(r_0, r_h = 0)|^2$ in an arbitrary unit (a.u.)) is mainly distributed on the Si atoms (cyan spheres) next to the hole.

The graphitic sheet along a specific lattice vector into a nanocylinder. This geometrical connection between a single-wall nanotube and the isolated sheet has inspired the application of the zone-folding method to construct the zeroth-order electronic band structure and phonon dispersions for single-wall nanotubes[11]. However, the zone-folding scheme alone cannot address the significant orbital rehybridization due to the curvature effect and the many-body interaction effects in the nanotubes mentioned above. To include these effects, we have calculated the diameter-dependence of the fundamental quasiparticle band gap of some small-radius zigzag and armchair SiC-NTs, as compiled in Fig. 4. First of all, we note that all the SiC-NTs are semiconductors, and this may be attributed to the different potentials of the Si and C atoms, being similar to the case of the BN nanotubes[13]. However, the zone-folding scheme alone cannot address the significant orbital rehybridization due to the curvature effect and the many-body interaction effects in the nanotubes mentioned above. To include these effects, we have calculated the diameter-dependence of the fundamental quasi-particle band gap of some small-radius zigzag and armchair SiC-NTs, as compiled in Fig. 4. First of all, we note that all the SiC-NTs are semiconductors, and this may be attributed to the different potentials of the Si and C atoms, being similar to the case of the BN nanotubes[13].

Secondly, an asymptotic convergence of the calculated band gaps of the zigzag and armchair SiC-NTs as a function of tube size towards that of the isolated SiC sheet is observed in both the LDA and GW calculations.

Interestingly, in contrast to the reciprocal radius dependence of the band gap in CNTs, we find a peculiar band gap reduction with the decrease of tube size for both zigzag and armchair SiC-NTs. This band gap reduction of SiC-NTs with the increasing tubular curvature can be attributed to the curvature-induced hybridization between the $\pi^*$ and $\sigma^*$ orbitals near the conduction band minimum (CBM) in the small radius SiC-NTs, similar to that found in the very small diameter CNTs.[46] To illustrate this point, we display the charge density contours of the CBM of the zigzag ($n,0$) and armchair ($n,n$) nanotubes at the 1D Brillouin zone center (Γ point) and zone boundary (Z point), respectively, in Fig. 5. Figure 5 shows that in the small zigzag ($n,0$) SiC-NTs such as (5,0) and (6,0) nanotubes, a strong mixture of the $\pi^*$ and $\sigma^*$ states in the SiC sheet now exists inside the tube to form a ring-like charge distribution, whereas the feature of the $p_z$ state is floating above the Si and C atoms outside the SiC-NT even under considerable structural distortion. Therefore, a substantial band gap reduction upon increasing the tube curvature can be expected. Indeed, this is confirmed by our LDA and quasiparticle calculations (see circle symbols in Fig. 4). In contrast, a much smaller degree of the orbital hybridization in the armchair SiC-NTs is induced by the folding-curvature, as revealed by the cylindrically symmetric distribution of the Si $p_z$ component of the CBM at the Brillouin zone boundary (Z point) in the (5,5) nanotube (Fig. 5). This

FIG. 4. (Color online) The fundamental band gaps of some zigzag ($n,0$) and armchair ($n,n$) SiC nanotubes as a function of the tube diameter from the GW (solid symbols) and LDA[17] (open symbols) calculations. The band gap of the isolated SiC sheet obtained from the GW and LDA calculations is also displayed as the solid and dashed line, respectively. Dotted lines between the symbols are a guide to the eye only.
FIG. 5. (Color online) The charge density contours ($\rho$ in $10^{-2} \text{Å}^{-3}$) of the states at the conduction band minimum (CBM) at the 1D Brillouin zone boundary (Z point) of the (3,3) and (5,5) SiC-NTs and also at the zone center (Γ point) of the (5,0) and (6,0) SiC-NTs. The Si and C atoms are represented by the cyan and yellow spheres, respectively.

gives rise to a minor size dependence of the band gap (square symbols in Fig. 4) for the armchair SiC-NTs. Nevertheless, a spectacular curvature effect in terms of strongly enhanced $\pi^* - \sigma^*$ hybridization does occur in the ultrasmall armchair (3,3) SiC-NT (see Fig. 5). This unusual orbital rehybridization effects on the band gap have also been recognized before in other ionic group III-V nanotubes[14, 45].

The quasiparticle corrections to the Kohn-Sham eigenvalues from the GW calculations for two ultrasmall (radius being $\sim 5 \text{ Å}$) armchair (3,3) and zigzag (5,0) SiC-NTs are given in Fig. 6, together with their LDA band structures. In the (3,3) SiC-NT, the GW corrections widens the LDA indirect band gap (2.13 eV) to the direct one of 4.09 eV, and also modify the band dispersions significantly as a result of the complicated energy dependence of the GW corrections (see open circles in Fig. 6). Meanwhile, the small direct band gap (0.19 eV) of the (5,0) SiC-NT predicted by the LDA is increased to 2.02 eV in the GW calculations. Furthermore, the GW corrections depend rather sensitively on the electronic state character, as illustrated in Fig. 6 for the (5,0) SiC-NT (open squares). We note that the curvature-induced hybridization between the $\pi$ and $\sigma$ states in these ultrasmall SiC-NTs is responsible for the mixture of the quasiparticle corrections of the otherwise orthogonal $\pi$ and $\sigma$ states near the top of the valence band in the SiC sheet. This hybridization would become weaker gradually as the tube radius increases, and eventually diminish in the large tube radius limit where the self-energy corrections would be the same as that of the SiC sheet (as shown Fig. 2). The NFE tubular states are found in both (3,3) and (5,0) tubes as well as the small-radius chiral SiC-NTs. However, these NFE states lie in the rather high energy region (more than 5 eV above the band gap region from the LDA calculations) and hence play a minor role in the optical absorption spectrum. Therefore, they are not included in the present GW and GW+BSE calculations. Nonetheless, the NFE states can be shifted downward toward the band gap regime by doping electrons in the nanotubes[48] and consequently may significantly affect the optical properties of the n-type SiC-NTs.

**EXCITONIC EFFECTS IN SiC NANOTUBES**

In quasi-one dimensional nanotube systems, the wavefunctions of quasielectrons and quasiholes can overlap significantly because of quantum confinement, and therefore, electron-hole interaction may be considerably en-
TABLE II. The binding energies ($E_B$) of the first bright exciton ($I_1$) and lowest energy dark exciton ($K_1$) below $I_1$ for the single-wall zigzag and armchair SiC nanotubes (NTs) considered here. The exciton binding energy ($E_B$) is calculated as the energy difference between the onset energy ($E$) of the corresponding interband transition continuum and the excitation energy ($\Omega$). The tube diameter ($D$) and quasiparticle energy gap ($E_{QP}^{gap}$) are listed for comparison. Symbol (i) denotes an indirect band gap in the armchair SiC-NTs. Moreover, the results for the SiC sheet which can be considered as the limiting case of an infinite diameter SiC-NT, are also listed for comparison. All the energies are in the unit of eV.

| NTs  | D (Å) | $E_{QP}^{gap}$ | $E^{I_1}$ | $\Omega^{K_1}$ | $\Omega^{I_1}$ | $E^K_B$ | $E^I_B$ |
|------|-------|---------------|----------|----------------|----------------|--------|--------|
| (3,3) | 5.05  | 4.09 (i)      | 4.86     | 2.86           | 2.00           |        |        |
| (4,4) | 7.43  | 3.81 (i)      | 4.75     | 3.12           | 1.63           |        |        |
| (5,5) | 8.45  | 4.15 (i)      | 4.55     | 3.13           | 1.42           |        |        |
| (5,0) | 5.10  | 2.02          | 2.02     | 0.28           | 3.21           | 1.64   | 1.71   |
| (6,0) | 6.06  | 2.51          | 2.51     | 5.70           | 0.95           | 4.24   | 1.56   | 1.46   |
| Sheet | ∞     | 4.42          | 4.42     | 3.25           | 1.17           |        |        |

enhanced. At the same time, the screening among the quasiparticles can be systematically changed because of curvature and reduced-dimensionality effects. For example, the phenomenon of anti-screening was discovered recently in the CNTs.[49] Therefore, the absorption features associated with the exciton formation can become prominent in the optical spectra in SiC-NTs. To study the excitonic effects on the optical properties of SiC-NTs, we have performed GW+BSE calculations by taking into account the electron-hole interaction kernel for several SiC-NTs of different sizes and different chiralities.

In Fig. 7, the quasiparticle band structure and the imaginary part of the optical polarizability for the ultrasmall armchair (3,3) SiC-NT are presented. Because of the strong depolarization effects in nanotubes[50], only the optical response for light polarized along the tube axis is significant. Therefore, only this polarization is considered here. For comparison, the optical absorption spectrum obtained without the electron-hole interaction in the GW+RPA scheme is also displayed in Fig. 7 (the blue-dashed curve in Fig. 7b). The onset energy (4.86 eV) of this independent-particle optical spectrum corresponds to the lowest-energy dipole-allowed vertical transition ($E^I_1$) from the valence to conduction bands near $2/3$ of the $\Gamma-Z$ line in the Brillouin zone which corresponds to the $K$ point in the hexagonal BZ of the SiC sheet (see Fig. 7a).

When the interaction between electrons and holes is included, excitons with specific excitation energies ($\Omega$) are formed to give rise to the prominent photoabsorption peaks. The binding energy of the lowest-energy exciton is defined as the energy difference between the continuum onset and corresponding excitation energy. For the armchair (3,3) SiC-NT, the optical absorption spectra from the GW+BSE calculations is dominated by the discrete exciton peaks [see the red curves in Fig. 7(b)]. The first bright exciton ($I_1$) appearing at 2.86 eV with a large binding energy ($E^I_1$) of $\sim 2.0$ eV is formed by a mix-
ture of four pair of interband transitions, as indicated by the arrows in Fig. 7(a). These four different interband transitions couple strongly to make the electron amplitude more localized and highly asymmetric around the hole position located outside the tube but near the C atom, as displayed in the inset in Fig. 7(b), thereby resulting in a strongly bound character of exciton $I_1$. At the same time, the large electron-hole overlap in the (3,3) SiC-NT lifts the double degeneracy of the $E_{1\pi-\pi^*}$ exciton in the 2D SiC sheet to create the bright $I_1$ exciton and a dark exciton with a higher (by 0.02 eV) excitation energy. Similar excitonic effects are also found in the larger armchair (5,5) SiC-NT (see Table II). However, the lowest optically active exciton in the (5,5) SiC-NT has a smaller binding energy of $E_B^{I_1} = 1.42$ eV, because the reduced electron-hole overlap due to the decreased curvature. Moreover, apart from the bright bound and resonant excitons shown as red peaks in Fig 7(b), there also exist many dark excitons among the bright ones. However, we find no dark exciton below the $I_1$ exciton in the armchair SiC-NT. As mentioned before, this can be anticipated from the fact that the isolated SiC layer has a direct band gap at the $K$-point. In this case, there is no momentum mismatch when the SiC sheet is rolled up to form an armchair SiC-NT, and hence the possibility of the formation of the optically inactive lowest-energy exciton diminishes[45].

Next, let us concentrate on the excitonic effects on the optical absorption in the small radius zigzag SiC-NTs. In order to scrutinize the chirality effects, we performed GW+RPA and GW+BSE calculations of the zigzag (5,0) SiC-NT with a tube radius comparable to that of the armchair (3,3) SiC-NT. The quasiparticle band structure and optical polarizability $\alpha_2$ of the (5,0) SiC-NT is displayed in Fig. 8 (a) and (b), respectively. In Fig. 8 (b), label $I_j$ denotes the $j$th optically allowed excited state. The inset in Fig. 8 (b) is a contour plot of the electron charge density distribution of the $I_1$ exciton with respect to a fixed hole position. Like the (3,3) SiC-NT, the photoexcited spectrum of the (5,0) SiC-NT is characterized by the discrete exciton peaks. The first bright exciton $I_1$ is the most prominent feature in the spectrum, and consists of the different interband transitions near the zone-center $\Gamma$-point (represented by the solid arrow). As a result, the charge density distribution is not cylindrically symmetric. Similar results are found in the (6,0) SiC-NT, and the corresponding excitation energies are listed in Table II. Interestingly, although the (5,0) and (3,3) SiC-NTs have a similar curvature, the relatively smaller binding energy (0.3 eV) of the $I_1$ exciton in the (5,0) SiC-NT indicates a rather delocalized exciton. This pronounced chirality effect can be attributed to the considerable orbital rehybridization in the zigzag SiC-NTs emphasized above. This orbital rehybridization induces a significant band-gap reduction giving rise to the increasing of the effective screening, and hence reduces the binding energy.

Furthermore, according to the zone-folding scheme for nanotubes, the lowest energy optically active interband transition at the $K$ point of the 2D sheet can be folded into the $\Gamma$ point to form a bright exciton with the lowest excitation energy in zigzag nanotubes. However, in the very small-radius zigzag SiC-NTs such as the (5,0) nanotube, the strong curvature-induced orbital rehybridization has brought a higher conduction band down to the GW band gap (0.0 \sim 4.0 eV) region [see Fig. 8 (a)]. Since the optical transitions from the top valence bands
to this conduction band are dipole-forbidden, some low energy dark excitons including the $K_1$ dark exciton, appear in the small-radius zigzag SiC-NTs. As shown in Table II, this low-energy $K_1$ dark exciton is also rather localized with a large binding energy, and this could make the zigzag SiC-NTs candidates for the tunable optical devices for temperature or external field sensors.

Finally, we explore the extent of the exciton wavefunction localization in the different SiC-NTs by comparing the intensity of their electron-hole wavefunctions in real space. In Fig. 9, the isosurface plots of the electron density with the fixed hole position (the red cross in the figure) of the first bright exciton ($I_1$) of the armchair SiC-NTs suggest a significant local distribution in the direction along the circumference of the tube. Mixing of excitations to different subband pairs in the small-radius SiC-NTs is responsible for this tightly bound character. In addition, a spatial localization of the exciton wavefunction along the tubular direction is also revealed by integrating out the electron coordinates in the perpendicular plane (red curves in Fig. 9). In contrast with the carbon nanotubes, the deviation from the one-dimensional nature of the low-energy exciton is mainly attributed to the strongly mixing of the interband transitions. Similar tightly bound behavior of the lowest-energy bright exciton has also been discovered in the BN-NTs [24]. In the zigzag SiC-NTs, we find the similar anisotropic bound nature of the first bright exciton. The slightly broadened distribution of the integrated wavefunction intensity (see the blue curves in Fig. 9) suggests a less bound character in the zigzag SiC-NTs. The distinct spiky features in the curve are located on the cation (Si atom) planes and they indicate a charge transfer from an anion (hole) to its neighboring cations by photoexcitation. On the other hand, the pronounced peak structures are not observed in the armchair SiC-NT because of the specific atomic arrangement dictated by its particular chirality. Furthermore, the asymmetric distribution of $|\Phi|^2$ with respect to the fixed hole position, is a consequence of the different nearest-neighbor cation-anion distances caused by rolling up the ideal symmetric 2D SiC sheet. This curvature-induced spatial symmetry breaking is also responsible for the special nodal-like feature near the hole position in the smallest armchair (3,3) SiC-NT. Nonetheless, by comparing the distribution of the exciton wavefunction of the (3,3) SiC-NT with the larger (5,5) nanotube, we note that this symmetry breaking will decrease gradually as the curvature decreases or the tube diameter increases.

CONCLUSIONS

In summary, we have employed the state-of-the-art many-body GW and GW+BSE approaches to study the quasiparticle band structure and optical properties, respectively, of the SiC sheet and related SiC nanotubes. First of all, we find a direct quasiparticle band gap for the isolated 2D SiC sheet. Our GW band structure calculations show that rather complicated orbital-dependent self-energy corrections are needed in obtaining accurate quasiparticle properties for the isolated SiC layer. The profile of the optical spectra is modified dramatically when the electron-hole interaction is included. In particular, a strongly bright bound exciton with a large binding energy (1.17 eV) is found to dominate the optical spectrum, because of the enhanced overlap between the electron and hole orbitals due to reduced-dimensionality effects and also the existence of vacuum region which reduces the effective screening in the SiC sheet.

Secondly, the quasiparticle band structure of the small-radius armchair and zigzag SiC-NTs is systematically studied within the GW approximation. Our detailed analysis on the charge density distributions reveals that a curvature-induced orbital rehybridization plays a vital role on determining the band gap of the small-radius SiC-NTs with different chiralities at both the LDA and GW levels. In particular, the quasiparticle band gaps as a function of tube diameter behave very differently, depending on the chirality of the SiC-NTs concerned.

Finally, the calculated photoexcited spectra are consisted of discrete exciton peaks, thereby indicating strong excitonic effects in both the armchair and zigzag SiC-NTs. The optical absorption spectra of the small radius
armchair and zigzag SiC-NTs are dominated by the first bright bound exciton \( I_1 \) with a significant binding energy up to \( \sim 2.0 \) eV. The highly asymmetric charge distribution of the exciton \( I_1 \) in the (3,3) SiC-NT is found to be a consequence of the strong coupling of the four optically allowed inter-subband transitions. Interestingly, we also find a quasi-zero dimensional bound character of the first bright exciton in the SiC-NTs and curvature-induced symmetry breaking affects the shape and size of this bound exciton. Moreover, our GW and BSE calculations demonstrate that the simple zone-folding approach fails in predicting the low energy exciton characters in very small zigzag SiC-NTs, mainly because of the strong curvature-induced orbital rehybridization in these nanotubes. We believe that the large excitation energy of \( \sim 3.0 \) eV of the first bright exciton, with no dark exciton below it, may make the small-radius armchair SiC-NTs candidates for optical devices working in the UV regime. In contrast, the numerous dark excitons below \( I_1 \) in the zigzag SiC-NTs may lead to potential applications in tunable optoelectric devices ranging from infrared to UV frequencies by external perturbations.

We thank Jack Deslippe for helpful discussions on performing the GW+BSE calculations in BerkeleyGW code. H. C. H. and G. Y. G. thank the National Science Council and NCTS of ROC for support, and also NCHC of ROC for CPU time. S.G.L. is supported by the Director, Office of Science, Office of Basic Energy Sciences, Materials Sciences and Engineering Division, U.S. Department of Energy under Contract No. DE-AC02-05CH11231.

* hchsuch@mail.tku.edu.tw
† gyguo@phys.ntu.edu.tw

[1] Semiconductors: Physics of Group IV Elements and III-V Compounds, Landolt-Börnstein, New Series, Group IV and III-V, Vol. 17, Pt. A, edited by K. H. Hellwege and O. Madelung (Springer-Verlag, Berlin, 1982).

[2] R. W. G. Wyckoff, Crystal Structures (Wiley, New York, 1963).

[3] P. A. Ivanov and V. E. Chelnokov, Semicond. Sci. Technol. 8, 763 (1992).

[4] C. Persson and U. Lindefelt, J. App. Phys. 82, 5496, (1997)

[5] R. Wang, D. Zhang, C. Liu, Chemical Phys. Lett. 411, 333, (2005).

[6] R. Rurali, P. Godignon, J. Rebollo, E. Hernandez, and P. Ordejon, Appl. Phys. Lett. 82, 4298 (2003).

[7] C. H. Park, B. H. Cheong, H. K. Lee, and K.J. Chang, Phys. Rev. B 49, 4485, (1994)

[8] Properties of Silicon Carbide edited by G. L. Harris (INSPEC, Institution of Electrical Engineers, London,1995)

[9] R. H. Sun, C.-P. Li, W.-K. Wong, N.-B. Wong, C.-S. Lee, S.-T. Lee, and B.-K. Teo, J. Am. Chem. Soc. 124, 14464 (2002).

[10] S. Iijima, Nature (London) 354, 56 (1991).

[11] R. Saito, G. Dresselhaus and M. S. Dresselhaus, Physical Properties of Carbon Nanotubes (Imperial College Press, London, 1998).

[12] G. Y. Guo, K. C. Chu, D. S. Wang, and C. G. Duan, Phys.Rev. B 69, 205416 (2004).

[13] A. Rubio, J. L. Corkill and and M. L. Cohen, Phys. Rev. B 49, 5081 (1994).

[14] G. Y. Guo and J. C. Lin, Phys. Rev. B 71, 165402 (2005).

[15] M. Zhao, Y. Y. Xia, D. J. Zhang and L. M. Mei, Phys. Rev. B 68, 235415 (2003).

[16] S. M. Lee, Y. H. Lee, Y. G. Hwang, J. Elsner, D. Porezag, and Th. Frauenheim, Phys. Rev. B 60, 7788 (1999).

[17] I. J. Wu and G. Y. Guo, Phys. Rev. B 76, 035343 (2007).

[18] I. J. Wu and G. Y. Guo, Phys. Rev. B 78, 035447 (2008).

[19] Y. Miyamoto and B. D. Yu, Appl. Phys. Lett. 80, 586 (2002).

[20] M. Menon, E. Richter, A. Mavromanolakis, G. Froudakis, and A. N. Andriotis, Phys. Rev. B 69, 115322 (2004).

[21] G. Y. Guo and J. C. Lin, Phys. Rev. B 72, 075416 (2005); 77, 049901 (E) (2008).

[22] G. Y. Guo, S. Ishibashi, T. Tamura, and K. Terakura, Phys. Rev. B 75, 245403 (2007).

[23] C. D. Spataru, S. Ismail-Beigi, L. X. Benedict, and S. G. Louie, Phys. Rev. Lett. 92, 077402 (2004).

[24] C.-H. Park and C. D. Spataru and S. G. Louie, Phys. Rev. Lett. 96, 126105 (2006).

[25] K. S. Novoselov, A. K. Geim, S. V. Morozov, D. Jiang, Y. Zhang, S. V. Dubonos, I. V. Grigorieva, and A. A. Firsov, Science 306, 666 (2004).

[26] A. H. Castro Neto, F. Guinea, N. M. R. Peres, K. S. Novoselov, and A. K. Geim, Rev. Mod. Phys. 81, 109 (2009).

[27] M. Rohlfing and S. G. Louie, Phys. Rev. Lett. 81, 2312 (1998).

[28] M. Rohlfing and S. G. Louie, Phys. Rev. B 62, 4927 (2000).

[29] W. Kohn and L. J. Sham, Phys. Rev. 140, A1133 (1965).

[30] M. S. Hybertsen and S. G. Louie, Phys. Rev. Lett. 55, 1418 (1985).

[31] M. S. Hybertsen and S. G. Louie, Phys. Rev. B 34, 5390 (1986).

[32] B. G. Pfrommer, M. Cote, S. G. Louie and M. L. Cohen, J. Comput. Phys. 131, 233 (1997).

[33] L. Kleinman and D. M. Bylander, Phys. Rev. Lett. 48, 1425 (1982).

[34] H. J. Monkhorst and J. D. Pack, Phys. Rev. B 13, 5188 (1976).

[35] I. Hedin, Phys. Rev. A39, 1796 (1965).

[36] W. G. Aulbur and L. Jonsson and J. W. Wilkins, Solid State Physics: Advances in Research and Applications vol. 54, p. 1 (Academic, New York, 2000).

[37] C. D. Spataru, S. Ismail-Beigi, R. B. Capaz and S. G. Louie, Carbon Nanotubes: Advanced Topics in the Synthesis, Structure, Properties and Applications vol. 111, p. 195 (Springer-Verlag, Heidelberg, 2008).

[38] J. B. Neaton, M. S. Hybertsen and S. G. Louie, Phys. Rev. Lett. 97, 216405 (2006).

[39] C. D. Spataru, S. Ismail-Beigi, L. X. Benedict and S. G. Louie, Appl. Phys. A 78, 1129 (2004).

[40] S. Ismail-Beigi, Phys. Rev. B 73, 233103 (2006).

[41] L. Yang, J. Deslippe, C.-H. Park, M. L. Cohen, and S. G. Louie, Phys. Rev. Lett. 103, 186802 (2009).

[42] H. Sahin, C. Cahangirov, M. Topsakal, E. Bekaroğlu, E. Akturk, R. T. Senger and S. Ciraci, Phys. Rev. B 80, 155453 (2009).
Here we have also performed the LDA, GW and BSE calculations for the bulk 2H SiC, and find the LDA and GW band gaps to be 2.10 and 3.17 eV, respectively. The BSE calculation predicts the exciton binding energy in 2H SiC to be 0.1 eV.

S. Ismail-Beigi, Phys. Rev. B 77, 035306 (2008).

X. Blase, L. X. Benedict, E. L. Shirley, and Steven G. Louie, Phys. Rev. Lett. 72, 1878 (1994)