Social-PatteRNN: Socially-Aware Trajectory Prediction Guided by Motion Patterns

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Abstract—As robots across domains start collaborating with humans in shared environments, algorithms that enable them to reason over human intent are important to achieve safe interplay. In our work, we study human intent through the problem of predicting trajectories in dynamic environments. We explore domains where navigation guidelines are relatively strictly defined but not clearly marked in their physical environments. We hypothesize that within these domains, agents tend to exhibit short-term motion patterns that reveal context information related to the agent’s general direction, intermediate goals and rules of motion, e.g., social behavior. From this intuition, we propose Social-PatteRNN, an algorithm for recurrent, multimodal trajectory prediction that exploits motion patterns to encode the aforesaid contexts. Our approach guides long-term trajectory prediction by learning to predict short-term motion patterns. It then extracts sub-goal information from the patterns and aggregates it as social context. We assess our approach across three domains: humans crowds, humans in sports and manned aircraft in terminal airspace, achieving state-of-the-art performance.

I. INTRODUCTION

Understanding and predicting the intended motion of humans in an environment is an important skill that robots across various domains, e.g., social robotics [1], [2], and aerial robotics [3], must be equipped with in order to enable safe interactions. Even beyond robotics, other domains such as surveillance [4] or sports analysis [5], [6] may also benefit from algorithms for modeling intent in dynamic scenes.

Motion and intent can be influenced by several factors, making the task challenging. One factor is social behavior, which describes how agents interact, and it heavily depends on the context. For instance, in a sports-based setting, e.g., a basketball game, close proximity to other agents may be a valid behavior, whereas in urban settings, e.g., pedestrians on a side walk, it may not. Respecting motion constraints is another relevant aspect in this setting, as it is related to restrictions that may arise from the agent’s own physical constraints, e.g., pedestrians may have more freedom of motion than a vehicle, while vehicles may move at higher speeds, or the constraints imposed by the environment, such as the topology of a scene, or the rules associated with it, e.g., pilots should respect flying guidelines. Moreover, agent motion is driven by each agent’s goals which vary depending on the situation and the type of agent: goals can be flexible or fixed, short or long-term, implicit or explicit. This varied nature makes them difficult to model.

The majority of existing works on trajectory prediction are mainly focused on pedestrian behaviors [7]–[10] where the context is relatively loosely defined, i.e., except for the social norm that pedestrians try to maintain the comfortable distance from others, there are few rules that guide pedestrian behavior. Moreover, the environmental context is largely ignored and few existing works, e.g., [11], [12] address that. Recent works show promising results by considering the goal context in their predictions [5], [13], [14].

In this paper, we specifically focus on the settings where there exist navigation guidelines relatively strictly defined yet not clearly marked in their physical environments, e.g., in aerial navigation, although there are strict rules analogous to ground navigation, the air space does not display visible lanes. To address this challenge, we propose an approach, known here as Social-PatteRNN, where we aim to learn such contexts in the form of motion patterns and social influences extracted from the patterns. Inspired by [10], we hypothesize that, within these domains, in the short term, agents tend to exhibit some motion patterns that reveal both their general directions of motion and their intermediate goals. We also believe that such patterns further explain general rules of motion, which may be explicit, e.g., sports rules or flying guidelines, or implicit, e.g., social etiquette, as well as, capture admissible motions. From these intuitions, we propose a data-driven approach to learn these patterns of motion and use them as a conditioning signal for predicting multimodal trajectories. Then, we use the learned patterns to extract sub-goal information which we aggregate to our model as the social context.

To assess the performance and the generalizability of the proposed approach across different domains, we evaluate it on three different scenarios: humans in crowds [5], [15], humans in sports [5], and manned aircraft [3]. Experimental results show that the proposed approach has consistent...
Fig. 2: An overview of Social-PatteRNN. We show an example of the data flow for Agent 1 during training (→), inference (−→), and both (→−→). Here, A Scene shows an example of a ground truth (GT) scene showing the locations, patterns and sub-goals of all agents at step t. B Backbone is the module used for generating locations and summarizing the trajectories. C Context Module produces the pattern and social features which form the context feature used as input to the backbone. Performance across these domains.

Our main contributions are: 1) we propose a generalizable approach for exploiting motion patterns for trajectory prediction; 2) we analyze the proposed approach via ablation to demonstrate the strength of each sub-component; 3) we open source Social-PatteRNN; and 4) we share our findings and insights on the sensitivity of the performance to the type of dataset and how it is used, and discuss future directions.

II. RELATED WORK

A. Modeling Techniques

Recent works tackle socially-aware trajectory prediction through data-driven methods [5], [7], [8], [10]. Here, three main aspects are generally taken into account. First, the use of temporal mechanisms for encoding sequences, such as Recurrent Neural Networks (RNN) [5], [7], [13], [14] and Temporal Convolutional Networks (TCN) [3], [10], [16], both of which have been shown to exhibit comparable performance [17]. Secondly, modeling the multi-modality of trajectories. For this, researchers have used generative frameworks such as Conditional Variational Autoencoders (C-VAE) [3], [5], [18], and Generative Adversarial Networks (GAN) [11], [19]. Thirdly, aggregating and modeling social behavior. Common approaches include using social pooling [7], [8] and attention-based models [5], [13], [20]. For instance, [7] uses a neighboring-based pooling over the hidden states of a given set of agents. However, as explained in [10], the drawback to this type of mechanism lies in the difficulty of understanding the semantic representation of hidden states generated by RNNs. Recent works have geared toward using Graph Attention Networks (GAT) to aggregate social context [3], [5], [13], showing performance improvements upon prior work. However, as highlighted by [21], [22], GAT models exhibit various limitations such as lack of expressiveness [21], and proneness to issues like over-fitting and over-smoothing [22]. Other recent approaches have shown promising results using Transformer-based methods [23] to model and attend over trajectory sequences [20], [24]. Inspired by these works, we use a self-attention mechanism [23] to model the dependencies between the social influences of all agents on the current agent (See Section III-E).

B. Exploiting Motion Patterns

Social Pattern Extraction Convolution (SPEC) [10] also uses motion patterns to learn a pattern scene and predict trajectories from it. Within human crowds, their idea works well because pedestrians tend to move linearly. However, we observed that this model does not generalize to different spatial domains, such as navigating in 3D space, or where motion is highly dynamic, e.g., sports. It also relies on various hyper-parameters for initializing the scene representation and it is sensitive to said initialization. Motivated by this idea, we also leverage motion patterns for trajectory prediction. However, instead of learning a fixed pattern scene, we equip the algorithm with a module that learns to predict patterns from current context information, and then uses them to extract social interactions. Our method uses motion patterns to guide the agents’ general direction based on the current state, as opposed to enforcing the motion. This is to account for unexpected behavior that may require agents to deviate from the prior intended direction. Finally, our algorithm is not sensitive to initialization and can be easily applied to different spatial domains.

III. THE APPROACH

We consider the problem of predicting the distribution of future trajectories of multiple agents in a shared environment, given the observations of their past trajectories and context
information. We first formulate this problem as estimating the conditional probability distribution over future trajectories, then, provide the technical details of the proposed approach.

A. Problem Formulation

The state of an agent \( i \) at time step \( t \), \( x^i_t \), represents the coordinates localizing the agent in a scene, e.g., \( x^i_t = (x, y, z) \). Its trajectory is defined as a sequence of \( T \) states, i.e., \( X^i = [x^i_1, x^i_2, \ldots, x^i_T] \). In our approach, we transforms the trajectories to relative motions, computed as the displacement between two consecutive steps, \( x^i_t \) and \( x^i_{t+1} \). For simplicity, we maintain the same notation for relative coordinates.

Within this problem setup, a trajectory is split into two segments; a history segment, \( X^i_H = [x^i_1, \ldots, x^i_T] \) and a future segment, \( X^i_F = [x^i_{T+1}, \ldots, x^i_F] \) of lengths \( H \) and \( F \), respectively. Then, we define the current context, \( c^i_t \), and the context history, \( C^i_H = [c^i_1, \ldots, c^i_T] \), as information that further describes the agent’s current state. For instance, context can be inferred from the observations, learned from previous experiences, or provided from external sources. In our approach, context refers to short-term motion patterns as well as social awareness relative to other agents which are both learned from training data.

The trajectory prediction problem is thus defined as finding the distribution of the future trajectories \( \hat{X}^i_F \) for each agent \( i \in \{1, \ldots, N\} \) in a scene, given their past trajectories and the context history. Formally,

\[
\hat{X}^i_F \sim p(X^i_F | X^i_H; C^i_H) \quad \forall i \in \{1, \ldots, N\}.
\]

B. An Overview of Social-PatteRNN

The proposed approach, known here as Social-PatteRNN, is an end-to-end model illustrated in Figure 2. Its backbone model consists of a recurrent encoder-decoder model denoted as VRNN in the figure, and the Location Extractor for mapping locations into a feature space.

Our innovations are focused on how context information is learned and used for prediction, i.e., in terms of motion patterns and social influences. Specifically, we propose the Context Module in Figure 2, consisting of: PatternNet, a module that learns to predict motion patterns given past context which are used to condition trajectory prediction during inference; and InteractionNet a module that exploits such motion patterns to further reflect social influences.

Our model can be easily be applied to various spatial navigation domains, e.g., human motions in 2D space or aircraft navigation in 3D. Moreover, its modularity enables to easily incorporate other contextual information.

C. Backbone Model

Following prior work [5], [13], [14], we adopt a recurrent version of the C-VAE, i.e., the Variational Recurrent Neural Network (VRNN) [25] for modeling the sequential nature of trajectories and their multi-modality. C-VAEs are an extension to the VAE [27], a type of generative model that is generally well-suited for representing multi-modal distributions by capturing the variations of the input data into a latent representation. C-VAEs allow to further condition on context variables as a method for controlling the generation process. RNNs capture the sequential dependencies in the data into hidden state variables.

The VRNN is trained as follows: first it takes a relative location at time-step \( t \) for agent \( i \), \( x^i_t \) and maps it into a feature space \( \bar{x}^i_t \). It then encodes the location feature along with a context feature \( \bar{c}^i_t \) and the previous hidden state \( h^i_{t-1} \) into a latent variable \( z^i_t \) which is then used by a decoder to reconstruct it into \( \hat{x}^i_t \). This is done for the entire history sequence \( X^i_H \) while also summarizing the hidden representation. During inference, the VRNN receives a history segment as before. Upon processing all history points, it obtains a final hidden state, \( h^i_F \), which is used to sample a future trajectory sequence of length \( F \), \( \hat{X}^i_F \).

The model consists of four main components, all of which are modeled as neural networks; the encoder (or posterior), \( p(\cdot) \), the decoder (or likelihood), \( q(\cdot) \), the prior, \( p_{\text{pr}}(\cdot) \), and the recurrent unit, \( \text{RNN}(\cdot) \). Additionally, the feature extractor modules for the input data, the latent space and the context vectors, denoted \( f^X(\cdot) \), \( f^C(\cdot) \), and \( f^Z(\cdot) \), respectively. In our paper, we denote features with a bar symbol, e.g., \( \bar{x}^i_t \). We note that \( f^X(\cdot) \) is implemented within the \( \odot \) VRNN, and we use \( f^Z(\cdot) \) to simplify notation as it rather refers to the modules introduced in sections III-D and III-E.

Mathematically, we can express the model as,

\[
\begin{align}
\bar{x}^i_t &= f^X(x^i_t) \\
\bar{c}^i_t &= f^C(c^i_t) \\
\bar{z}^i_t &= p(z_t | \bar{x}^i_t \oplus \bar{c}^i_t \oplus h_{t-1}) \quad \text{during training} \\
\hat{x}^i_t &= p_{\text{pr}}(z_t | h_{t-1}) \quad \text{during inference} \\
\hat{z}^i_t &= q(z_t | \bar{x}^i_t \oplus \bar{c}^i_t \oplus h_{t-1}) \\
h^i_t &= \text{RNN}(\bar{x}^i_t \oplus \bar{z}^i_t \oplus h_{t-1})
\end{align}
\]

where for all agents \( i \in \{1, \ldots, N\} \) at a given time step \( t \), Eq. 1 and Eq. 2 represent the location and context feature extractor networks, respectively. Eq. 3 and Eq. 4 show the encoder and prior networks, which are needed for learning a latent space \( Z \) and for sampling a corresponding latent representation \( z_t \in Z \) conditioned on the extracted features and the RNN’s hidden states. The encoder is used only during training to guide the prior—which does not have access to the input data—toward the latent space, enabling it to generate future trajectories during the inference stage. The decoder network is expressed in Eq. 6. It is in charge of reconstructing the location \( \hat{x}_t \) conditioned on the latent variable and context features. The RNN in Eq. 7 produces the hidden representation of the current time step using the extracted features and previous state information.

The loss function for optimizing the VRNN is:

\[
\begin{align}
L &= \sum_{t=1}^{H} \left[ \log q(z_t | \bar{x}^i_t \oplus \bar{c}^i_t \oplus h_{t-1}) \right] \\
D_{KL}(p(\bar{z}^i_t | \bar{x}^i_t \oplus \bar{c}^i_t \oplus h_{t-1}) \| p_{\text{pr}}(z_t | \bar{x}^i_t \oplus \bar{c}^i_t \oplus h_{t-1}))
\end{align}
\]

The first term represents the log-likelihood for reconstructing the input location while the second is the KL-divergence.
between the encoder and the prior distributions. For details regarding this equation, we refer the reader to [26], [27].

Distinguished from previous works, we condition the VRNN not only on the input data but also on a context feature which embeds features from short-term motion patterns, \( p_i^t \), and agent-to-agent interactions, \( s_i^t \). Sections III-D and III-E further describe these context features.

D. Learning Motion Patterns

Our approach is based on the intuition that social interactions in navigation are more local (short-term) rather than global (long-term) ones. Whereas previous approaches [3], [5], [14] use the agents’ long-term goals as the context to guide the learning process, we use short-term motion patterns to learn rules of motion, e.g., social behavior (Section III-E).

In our work, a motion pattern consists of a short trajectory sequence of length \( P \), where \( P \) is a hyperparameter. A pattern can be represented as absolute coordinates, relative displacements, or controls such as accelerations. Here, we represent it as a sequence of relative displacements from a given location \( x_i^t \), i.e., \( p_i^t = [x_i^t, \ldots, x_i^{t+P}] \). A Scene in Figure 2 depicts an example of the pattern representation.

We obtain pattern features, \( \hat{p}_i \), from motion patterns using the \( \bigcirc \) Pattern Extractor in Figure 2. Mathematically,

\[
\hat{p}_i^t = f^p(p_i^t)
\]

As explained in prior sections, the pattern features form part of the context feature vector used for training the VRNN.

During inference, since we aim to generate new data, we do not have direct access to pattern information. To address this, we train a neural network to predict future motion patterns given the previous pattern information and hidden state. We refer to this mechanism. Here, we refer to the latter feature extractor as \( \bigcirc \) InteractionNet.

\[
\mathcal{S}_i^t = \text{InteractionNet}(\bar{S}_i^t)
\]

Now, we can finally define the context feature vector introduced in Section III-A as \( \mathbf{c}_{ij}^t = \bar{p}_{ij} \oplus \mathcal{S}_i^t \). As shown in Figure 2, context features are fed to the VRNN backbone. We also feed the context vector to the previously introduced \( \bigcirc \) PatternNet. Thus, Eq. 9 now becomes,

\[
\hat{p}_{ij}^t = \text{PatternNet}(\bar{p}_{ij-1}, \mathbf{h}_{ij-1}^t)
\]

Finally, the full loss function for optimizing our model is,

\[
L_{\text{total}} = L_{\text{pat}} + L_{\text{cvae}}
\]

IV. Experiments

A. Datasets

We evaluate our model on the following datasets:

1) TrajAir [3]: A dataset designed for studying social navigation in non-towered airspace. It consists of 111 days of manned aircraft trajectory data. In [3], the authors train their model on a subset consisting of 28 days of data. We consider the 111 days of data; but, we partition the dataset differently. Since the dataset is heavily unbalanced toward single agent scenes (Table I), and we are interested in modeling social behavior in scenes with multiple aircraft, we train our models on a subset where scenes contain at least 4 agents.

| # agents | all 1 2 3 4 5 |
| --- | --- | --- | --- | --- | --- |
| # trajectories 425 / 177 | 298 / 177 | 90 / 42 | 26 / 14 | 9 / 3 | 2 / 0.2 |

2) Stanford Drone Dataset (SDD) [15]: A dataset consisting of top-down videos capturing social behavior in complex and crowded scenarios with different types of agents, e.g., pedestrians, bikers, skateboarders, and vehicles. We use the version in [5] where only pedestrians are considered.

3) SportVU NBA Dataset (NBA) [6]: A dataset collected with a SportVU system [6] consisting of motion tracking data of 10 basketball players; 5 attackers and 5 defenders. We use the version of NBA as in [5]. In [5], models are trained on each team separately as they consider the nature of the teams to be intrinsically different. We train on both teams jointly as we argue that agent behaviors influence the interactions within their own team as well as the opponent team.
B. Evaluation

Following prior work on trajectory prediction [3], [5], [7]–[10], [13], [14], we consider Average Displacement Error (ADE) and Final Displacement Error (FDE) as our metrics for assessing performance of our models. We first evaluate our approach by ablating its components. Specifically, we validated the backbone consisting of the VRNN, the use of motion patterns without social context (PAT), aggregating social interactions (SOC), and finally, attending over the interactions (ATT). Then, we evaluate Social-PatteRNN against four related models: A-VRNN [5], DAG-Net [5], SPEC [10], and TrajAirNet [3]. We adapted DAG-Net and SPEC for 3D space, and TrajAirNet for 2D.

C. Implementation Details

We used the VRNN in [5]. The feature extractors as well as PatternNet were implemented as fully-connected networks. For the attention mechanism in the InteractionNet we used 4 attention heads. We use Adam optimizer and train for at most 1000 epochs with and learning rate of $1e-3$ and early stopping. For the SDD and NBA datasets, we followed [5], where trajectories are split into $H = 8$ and $F = 12$, and $H = 10$ and $F = 40$, respectively. Empirically, we set the pattern lengths for SDD to $P = 6$ and for NBA to $P = 8$. For TrajAir, we use trajectory segments of 140 seconds and split them into $H = 40$ and $F = 100$ sampled every 5 steps, and pattern lengths of $P = 20$s [3].

V. RESULTS

A. Ablation Study

As explained in section IV-B, we validated the benefit of each component of the model by performing ablations. The corresponding results, summarized in Table II, show that using the pattern learning module improves the results in term of displacement errors in the three datasets. Moreover, exploiting pattern information to aggregate social features, achieves further reductions in error. We note that the more pronounced improvements correspond to TrajAir's results, where, adding pattern learning reduces ADE / FDE by $\sim 12/9\%$, while aggregating social features further improves these metrics by $\sim 5\%$. We find this specially relevant since in aircraft navigation, pilots are expected to follow flying patterns in addition to procuring safe interactions with other pilots [3]. We also observe that in the sports domain, where interactions are more frequent, aggregating social encoding achieves more significant improvements in ADE / FDE, of $\sim 11/14\%$, than only considering motion patterns, $\sim 3/2\%$.

B. Main Results

Figure 1 shows a qualitative result for the TrajAir dataset. In this example, we can observe that the predicted trajectories for TrajAirNet and the VRNN baseline do not align with the correct direction of the ground truth trajectory, while our models that were conditioned on additional context do. We can also observe that while the end-point of the trajectory predicted by DAG-Net gets close to the goal location, it does not follow the expected aircraft pattern, whereas our pattern-conditioned approaches do. Furthermore, our pattern-based models achieve smoother predictions than TrajAirNet and DAG-Net. We believe that these observations support our initial hypothesis that through motion patterns additional context information can be learned, e.g., general direction and rules of motion. Quantitatively, Table III summarizes the results for the socially-aware baselines introduced in Section IV-B and ours, which we show as Social-PatteRNN and Social-PatteRNN (ATT), for the models without and with attention, respectively. From these results we observe that our models outperform existing baselines in both TrajAir and NBA, and achieves comparable performance in the SDD dataset w.r.t to the state-of-the-art model, DAG-Net. As an additional finding, we observe that the performances of SPEC and DAG-Net, developed for human data, degrades on the aerial navigation dataset, while TrajAirNet, developed for aerial navigation, falls behind on human datasets.

VI. CONCLUSIONS

In our work, we hypothesized that short-term motion patterns reveal context information related to the agents' general direction, rules of motion, and how they interact with each other. From this intuition, we introduced Social-PatteRNN, a trajectory prediction algorithm that leverages motion patterns to capture these contexts. Our experiments show that the performance of existing approaches are sensitive to problem domain and how the dataset is composed. The results support our intuition that short-term patterns are robust indicators for trajectory prediction and are also less sensitive to problem domains. As future work, we aim to explore various avenues.
We are interested in further exploiting and learning the dependencies between the agents by exploring other trajectory data. Finally, we plan to extend our work to develop a safe and socially-aware robot navigation algorithm for urban driving and aerial navigation in crowded scenarios.

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REFERENCES
[1] S. Thrun, M. Bennewitz, W. Burgard, A. B. Cremers, F. Dellaert, D. Fox, D. Hähnel, C. R. Rosenberg, N. Roy, J. Schulte, and D. Schulz, “MINERVA: A second-generation museum tour-guide robot,” in 1999 IEEE International Conference on Robotics and Automation, Marriott Hotel, Renaissance Center, Detroit, Michigan, USA, May 10-15, 1999, Proceedings. IEEE Robotics and Automation Society, 1999, pp. 1999-2005.
[2] C. I. Mavrogiannis, F. Baldini, A. Wang, D. Zhao, P. Trautman, A. Steinfeld, and J. Oh, “Core challenges of social robot navigation: A survey,” CoRR, vol.abs/2103.05668, 2021.
[3] J. Patrikar, B. G. Moon, J. Oh, and S. A. Scherer, “Predicting like A pilot: Dataset and method to predict socially-aware aircraft trajectories in non-towered terminal airspace,” CoRR, vol.abs/2109.15158, 2021.
[4] S. Oh, A. Hoogs, A. Perera, N. Cuntoor, C.-C. Chen, J. T. Lee, S. Mukherjee, J. K. Aggarwal, H. Lee, L. Davis, E. Swears, X. Wang, Q. Ji, K. Reddy, M. Shah, C. Vondrick, H. Pirsiavash, D. Ramanan, J. Yuan, A. Torralba, B. Song, A. Fong, A. Roy-Chowdhury, and M. Desai, “A large-scale benchmark dataset for event recognition in surveillance video,” in CVPR 2011, 2011, pp. 3153-3160.
[5] A. Monti, S. Calderara, and R. Cucchiara, “Dog-net: Double attentive graph neural network for trajectory forecasting,” in 25th International Conference on Pattern Recognition, ICPAR 2020, Virtual Event / Milan, Italy, January 10-15, 2021, IEEE, 2020, pp. 2551-2558.
[6] “STATS Perform - SportVU NBA Dataset,” https://www.statsperform.com/team-performance/basketball/optical-tracking/.
[7] A. Alahi, K. Goel, V. Ramanathan, A. Robicquet, L. Fei-Fei, and S. Savarese, “Social LSTM: human trajectory prediction in crowded spaces,” in 2016 IEEE Conference on Computer Vision and Pattern Recognition, CVPR 2016, Las Vegas, NV, USA, June 27-30, 2016, IEEE Computer Society, 2016, pp. 961-971.
[8] A. Gupta, J. Johnson, L. Fei-Fei, S. Savarese, and A. Alahi, “Social GAN: socially acceptable trajectories with generative adversarial networks,” in 2018 IEEE Conference on Computer Vision and Pattern Recognition, CVPR 2018, Salt Lake City, UT, USA, June 18-22, 2018, Computer Vision Foundation / IEEE Computer Society, 2018, pp. 2255-2264.
[9] A. Vemula, K. Muellling, and J. Oh, “Social attention: Modeling attention in human crowds,” in 2018 IEEE International Conference on Robotics and Automation, ICRA 2018, Brisbane, Australia, May 21-25, 2018, IEEE, 2018, pp. 1-7.
[10] D. Zhao and J. Oh, “Noticing motion patterns: A temporal CNN with a novel convolution operator for human trajectory prediction,” IEEE Robotics Autom. Lett., vol. 6, no. 2, pp. 628-634, 2021.
[11] A. Sadeghian, V. Kosaraju, A. Sadeghian, N. Hirose, H. Rezatofighi, and S. Savarese, “Sofie: An attentive GAN for predicting paths compliant to social and physical constraints,” in IEEE Conference on Computer Vision and Pattern Recognition, CVPR 2019, Long Beach, CA, USA, June 16-20, 2019, Computer Vision Foundation / IEEE, 2019, pp. 1349-1358.
[12] T. Salzmann, B. Ivanovic, P. Chakravarty, and M. Pavone, “Trajectron++: Dynamically-feasible trajectory forecasting with heterogeneous data,” in Computer Vision - ECCV 2020 - 16th European Conference, Glasgow, UK, August 23-28, 2020, Proceedings, Part XVIII, ser. Lecture Notes in Computer Science, A. Vedaldi, H. Bischof, T. Brox, and J. Frahm, Eds., vol. 12363. Springer, 2020, pp. 683–700.
[13] C. Liu, Y. Chen, M. Liu, and B. E. Shi, “AVGCN: trajectory prediction using graph convolutional networks guided by human attention,” in IEEE International Conference on Robotics and Automation, ICRA 2021, Xi’an, China, May 30 - June 5, 2021. IEEE, 2021, pp. 14 234–14 240.
[14] K. Mangalam, H. Girase, S. Agarwal, K. Lee, E. Adeli, J. Malik, and A. Gaidon, “It is not the journey but the destination: Endpoint conditioned trajectory prediction,” in Computer Vision - ECCV 2020 - 16th European Conference, Glasgow, UK, August 23-28, 2020, Proceedings, Part II, ser. Lecture Notes in Computer Science, A. Vedaldi, H. Bischof, T. Brox, and J. Frahm, Eds., vol. 12347. Springer, 2020, pp. 759–776.
[15] A. Robicquet, A. Alahi, A. Sadeghian, B. Anenberg, J. Doherty, E. Wu, and S. Savarese, “Forecasting social navigation in crowded complex scenes,” CoRR, vol.abs/1601.00998, 2016.
[16] N. Nikhil and B. T. Morris, “Convolutional neural network for trajectory prediction,” in Computer Vision - ECCV 2018 Workshops - Munich, Germany, September 8-14, 2018, Proceedings, Part III, ser. Lecture Notes in Computer Science, L. Leal-Taixé and S. Roth, Eds., vol. 11131. Springer, 2018, pp. 186–196.
[17] S. Bai, J. Z. Kolter, and V. Koltun, “An empirical evaluation of generic convolutional and recurrent networks for sequence modeling,” CoRR, vol.abs/1803.01271, 2018.
[18] A. Bhattacharyya, M. Hanselmann, M. Fritz, B. Schiele, and C. Struwehl, “Conditional flow variational autoencoders for structured sequence prediction,” CoRR, vol.abs/1908.09008, 2019.
[19] H. Zou, H. Su, S. Song, and J. Zhu, “Understanding human behaviors in crowds by imitating the decision-making process,” in Proceedings of the Thirty-Second AAAI Conference on Artificial Intelligence, (AAAI-18), the 30th innovative Applications of Artificial Intelligence (IAAI-18), and the 8th AAAI Symposium on Educational Advances in Artificial Intelligence (EAAI-18), New Orleans, Louisiana, USA, February 2-7, 2018, S. A. McIlraith and K. Q. Weinberger, Eds. AAAI Press, 2018, pp. 7648–7656.
[20] Y. Yuan, X. Weng, Y. Ou, and K. Kitani, “Agentformer: Agent-aware transformers for socio-temporal multi-agent forecasting,” CoRR, vol.abs/2103.14023, 2021.
[21] S. Brody, U. Alon, and E. Yahav, “How attentive are graph attention networks?” CoRR, vol.abs/2105.14491, 2021.
[22] G. Wang, R. Ying, J. Huang, and J. Leskovec, “Improving graph attention networks with large margin-based constraints,” CoRR, vol.abs/1910.11945, 2019.
[23] A. Vaswani, N. Shazeer, N. Parmar, J. Uszkoreit, L. Jones, A. N. Gomez, L. Kaiser, and I. Polosukhin, “Attention is all you need,” in Advances in Neural Information Processing Systems 30: Annual Conference on Neural Information Processing Systems 2017, December 4-9, 2017, Long Beach, CA, USA, I. Guyon, U. von Luxburg, S. Bengio, H. M. Wallach, R. Fergus, S. V. N. Vishwanathan, and R. Garnett, Eds., 2017, pp. 5998–6008.
[24] F. Giuliani, I. Hasan, M. Cristani, and F. Galasso, “Transformer networks for trajectory forecasting,” CoRR, vol.abs/2003.08111, 2020.
[25] J. Chung, K. Kastner, L. Dinh, K. Goel, A. C. Courville, and Y. Bengio, “A recurrent latent variable model for sequential data,” in Advances in Neural Information Processing Systems 28: Annual Conference on Neural Information Processing Systems 2015, December 7-12, 2015, Montreal, Quebec, Canada, C. Cortes, N. D. Lawrence, D. D. Lee, M. Sugiyama, and R. Garnett, Eds., 2015, pp. 2980–2988.
[26] K. Sohn, H. Lee, and X. Yan, “Learning structured output representation using deep conditional generative models,” in Advances in Neural Information Processing Systems 23: Annual Conference on Neural Information Processing Systems 2010, December 7-12, 2010, Vancouver, British Columbia, Canada, J. D. Lee, M. Sun, S. Sugiyama, and R. Garnett, Eds., 2010, pp. 1409–1416.
[27] D. J. Rezende, S. Mohamed, and D. Wierstra, “Stochastic backpropagation and approximate inference in deep generative models,” in Proceedings of the 31th International Conference on Machine Learning, ICML 2014, Beijing, China, 21-26 June 2014, ser. JMLR Workshop and Conference Proceedings, vol. 32. JMLR.org, 2014, pp. 1278–1286.