A Novel Global MPP Tracking of Photovoltaic System based on Whale Optimization Algorithm

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ABSTRACT. To harvest maximum amount of solar energy and to attain higher efficiency, photovoltaic generation (PVG) systems are to be operated at their maximum power point (MPP) under both variable climatic and partial shaded condition (PSC). From literature most of conventional MPP tracking (MPPT) methods are able to guarantee MPP successfully under uniform shading condition but fails to get global MPP as they may trap at local MPP under PSC, which adversely deteriorates the efficiency of Photovoltaic Generation (PVG) system. In this paper, a novel MPPT based on Whale Optimization Algorithm (WOA) is proposed to analyze analytic modeling of PV system considering both series and shunt resistances for MPP tracking under PSC. The proposed algorithm is tested on 6S, 3S2P and 2S3P Photovoltaic array configurations for different shading patterns and results are presented. To compare the performance, GWO and PSO MPPT algorithms are also simulated and results are also presented. From the results, it is noticed that proposed MPPT method is superior to other MPPT methods with reference to accuracy and tracking speed.

Keywords: Maximum power point tracking, Partial shaded condition, Photovoltaic generation system, Single diode model, Whale optimization algorithm.

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1. Introduction

Due to dearth of fossil fuels and escalate load demand, renewable energy plays a crucial role in future power generation. Photovoltaic generation system is a popular renewable energy source which is inexhaustible and available in most regions of the world and proved to be a reasonably priced source of energy. To harvest maximum amount of solar energy, PVG systems are forced to operate at maximum power point (MPP) under both variable climatic and partial shaded condition (PSC) in conjunction with a power electronic converter. When PVG systems are subjected to uniform irradiation condition conventional MPPT controllers can efficiently track MPP (Kamarzaman et al. 2014, Reisi et al. 2013). But, when PVG system is subjected to PSC (due to passing clouds, tree branches, building shadows, etc.), it’s current-voltage (I-V) and power-voltage (P-V) characteristics exhibits many local maximum power points (LMPP) and only one global maximum power point (GMPP) due to bypass diode operation across the shaded modules (Silvestre et al. 2009). Many of the conventional MPPT algorithms cannot differentiate between LMPP and GMPP and thus they trap at one of the LMPP which adversely deteriorates the efficiency of PVG systems (Ishaque et al. 2013).

Several researchers proposed various soft computing based MPPT algorithms (Salam et al. 2013). Out of which meta-heuristic optimization algorithm based MPPT techniques like Particle Swarm Optimization (PSO) (Ishaque et al. 2012 – Liu et al. 2012), Artificial Bee Colony (ABC) (Benyoucef et al. 2015, Sundareswaran et al. 2015), Ant Colony Optimization (ACO) (Jiang et al. 2013), Differential Evolution (DE) (Tajuddin et al. 2013), Cuckoo Search

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2. Modeling of PV system under PSC

2.1 PV module

Several mathematical models of photovoltaic (PV) cell are proposed by researchers, out of which single diode model (SDM) is more predominantly used for PV cell modeling due to its simplicity and computational efficiency (Ma et al. 2014). The single diode model of PV module is presented in Fig. 1.

\[
I = I_{ph} - I_o \left[ \frac{V + IR_s}{V_t} - 1 \right] - \frac{V + IR_s}{R_{sh}} \tag{1}
\]

where \(I\) is PV output current, \(I_{ph}\) is the Photo current of module, \(I_o\) is the Diode saturation current, \(V\) is PV output voltage, \(R_s\) and \(R_{sh}\) are the series and shunt resistances.

\[
V_t = \frac{N_c K T A}{q} \tag{2}
\]

\[
I_{ph} = \left( I_{sc, stc} + k_i \Delta T \right) G \tag{3}
\]

where \(V_t\) is the thermal voltage of PV module, \(N_c\) is Number of cells in series in a module, \(q\) is the Charge of an electron (1.6 x 10^{-19} C), \(A\) is the Diode ideality factor, \(K\) is the Boltzmann’s constant (1.38 x 10^{-23} N-m/K), \(T\) is the Panel operating temperature (in Kelvin), \(I_{sc, stc}\) is the short circuit current at standard test conditions (STC), \(k_i\) is the current temperature coefficient, \(\Delta T\) is the temperature change (\(\Delta T=T-T_{stc}\)) in Kelvin and \(G\) is the solar irradiation in kW/m².

\[
I_o = I_{o, stc} \left( \frac{T_{stc}}{T} \right)^3 \exp \left[ \frac{-q E_g}{A k T_{stc}} \left( \frac{1}{T} - \frac{1}{T_{stc}} \right) \right] \tag{4}
\]

\[
I_{o, stc} = \frac{I_{sc} \exp \left( \frac{-q V_{oc}}{N_s A K T_{stc}} \right)}{1} \tag{5}
\]

where \(E_g\) is the bandgap energy (eV), \(V_{oc}\) is the open circuit voltage and \(I_{sc}\) is the short circuit current of PV module.

Equation (1) in terms of voltage function can be represented as:

\[
f(V, I) = V - I_{ph} R_{sh} + I_o R_{sh} \left( \exp \left( \frac{V + IR_s}{V_t} \right) - 1 \right) + I (R_s + R_{sh}) \tag{6}
\]

Equation (6) is non-linear with two variables \(V, I\) can be solved by Newton’s iterative method. The PV module parameters used for modeling the PV system are given in Table 1.

| Tabel 1 | Parameters for Kyocera KC-200GT module |
|---------|--------------------------------------|
| Maximum power (P_{mp}) | 200 W |
| Open circuit voltage (V_{oc}) | 32.9 V |
| Short circuit current (I_{sc}) | 8.21 A |
| Maximum power Voltage (V_{mp}) | 26.3 V |
| Maximum power current (I_{mp}) | 7.61 A |
| Voltage temperature coefficient (k_v) | -1.23 x 10^{-1} V/°C |
| Current temperature coefficient (k_i) | 3.18 x 10^{-3} A/°C |
2.2 PSC Modeling

In this work a system with 6S (Six series), 3S2P (Three series two parallel) and 2S3P (Two series three parallel) PV configurations as shown in Fig. 2 are modeled using the following equations:

\[ I = \sum_{k=1}^{s} I^k_s \]  
\[ V_{kn} = \begin{cases} 0 & \text{if } I^{kn} > I^k_s \\ V - \frac{I^{kn} R_s + I^k R_s}{V} (1 + \frac{V^{kn} + I R_s}{V}) - 1 & \text{if } I^{kn} \leq I^k_s \end{cases} \]  
\[ V_s^k = \sum_{n=1}^{m} V_{kn} \]

where \( s \) is number of parallel connected strings in an array. For detailed explanation refer (Alajmi et al. 2013).

3. WOA and its application for MPPT

3.1 Overview of WOA

Whale optimization algorithm is inspired from bubble net hunting strategy of humpback whales proposed by (Mirjalili et al. 2016). Humpback whale is the biggest of all whales and it has special hunting mechanism of spiral bubble-net feeding. These whales hunt the school of fishes or krill’s on the surface by creating distinctive bubbles in circular path as depicted in Fig. 3.

\[ D = \begin{cases} C \cdot \bar{X}^+ (k) - \bar{X}^{\star} (k) \\ D = \begin{cases} C \cdot \bar{X}^+ (k) - \bar{X}^{\star} (k) \\ C = 2\bar{\bar{r}} \end{cases} \]  
where \( \bar{\bar{r}} \) is the random vector between \([0,1]\). Here we refer \( X^{\star} \) as the best solution with knowledge about the prey location.
3.2 Application of WOA for MPPT

Here MPPT is formulated as objective function and it is represented as follows:

Maximize \( P(d) \) \hspace{2cm} (14)

Subjected to \( d_{\text{min}} \leq d \leq d_{\text{max}} \) \hspace{2cm} (15)

where \( P \) is PV output power, \( d \) is duty ratio, \( d_{\text{min}} \) is the minimum and \( d_{\text{max}} \) is the maximum limits of duty ratio i.e., 0.1 and 0.9, respectively. The block diagram for MPPT of PV system is depicted in Fig. 4.

![Figure 4: Block diagram for MPPT of PV system](image)

In this work WOA is implemented as a direct control MPPT technique i.e., duty cycle control by taking population of whales as duty ratios to reduce steady state oscillations. Direct control MPPT decreases power loss and therefore improves efficiency of the system. For each population of whales, i.e., duty ratios, the corresponding voltage and currents are sensed by the controller and compute output power.

For MPPT, (11) can be remodeled as

\[ d_i(k+1) = d_i(k) - A.D \] \hspace{2cm} (16)

The objective function of WOA MPPT is formulated as

\[ P(d_i^k) > P(d_i^{k-1}) \] \hspace{2cm} (17)

where \( i \) is the population of whales

PV power is dependent on climatic conditions, for a change in solar irradiation of PV modules, the power output of PV array changes correspondingly and proposed MPPT algorithm is reinitialized by sensing the change in PV output power using (18).

\[ \frac{P^k - P^{k-1}}{P^k} \geq 0.1 \] \hspace{2cm} (18)

The detailed methodology of proposed WOA MPPT algorithm is presented in Fig. 5.

4. Results and discussions

To examine the performance of proposed WOA MPPT algorithm, it is implemented for different combinations of PV configurations of six PV modules.

The shading patterns (W/m\(^2\)) of 6S PV configuration are as follows:

1) \( G_1, G_2=1000, G_3,G_4=600, G_5,G_6=200 \)
2) \( G_1=1000, G_2=800, G_3=600, G_4=400, G_5=200, G_6=100 \)

The shading patterns of 3S2P PV configuration are as follows:

3) \( G_1=1000, G_2=500, G_3=200, G_4=1000, G_5=600, G_6=200 \)
4) \( G_1=1000, G_2=400, G_3=200, G_4=1000, G_5=500, G_6=300 \)

![Figure 5: Flow chart for WOA MPPT Algorithm](image)
The shading patterns of 2S3P PV configuration are as follows:

5) \( G_1=1000, G_2=600, G_3=1000, G_4=600, G_5=1000, G_6=600 \)

6) \( G_1=1000, G_2=300, G_3=1000, G_4=200, G_5=1000, G_6=100 \)

4.1 PV configuration 6S

The P-V characteristics of 6S PV configuration for shading patterns 1 and 2 are shown in Fig. 6. These characteristics exhibit multiple maxima due to bypass diode operation across shaded modules, out of which only one is GMPP. In order to attain maximum benefit, the PV system should be operated at GMPP. This can be achieved by using the proposed MPPT technique.

The dynamic performance of the proposed algorithm is observed by operating the PV system at different shading patterns. The 6S PV configuration is subjected to pattern 1 from 0 to 30s and pattern 2 from 30s onwards. The algorithm reinitializes the search for change in shading pattern by sensing the change in the PV power. The tracking curves of proposed WOA MPPT algorithm for shading patterns 1 and 2 of 6S PV configuration are presented in Fig. 7.

From Fig. 7, it is clear that MPP tracking subjected to shading pattern 1 and 2 can be achieved by proposed MPPT algorithm. The maximum power extracted by proposed algorithm for pattern 1 is 394.52 W and the time for tracking the MPP is 5.4 s and at t=30 s algorithm reinitializes the search due to change in PV power, for pattern 2 the maximum power is 301.9 W and the time of tracking the MPP is 5.5 s. For comparative analysis, the proposed algorithm is compared with most recent GWO MPPT algorithm (Satyajit et al. 2016), and most implemented PSO MPPT algorithm (Ishaque et al. 2012) under similar conditions. The parameters of the three algorithms are given in Appendix. For fairness of comparison same number of population \( i \) is considered for all the algorithms.

4.2 PV configuration 3S2P

The P-V characteristics of 3S2P PV configuration for shading patterns 3 and 4 are shown in Fig. 8. The 3S2P PV configuration is subjected to pattern 3 from 0 to 30s and pattern 4 from 30s onwards. The proposed algorithm tracks the global MPP for both shading patterns. The tracking curves of proposed MPPT algorithm for shading patterns 3 and 4 of 3S2P PV configuration are presented in Fig. 9.

From Fig. 9 it is clear that MPP tracking subjected to shading pattern 3 and 4 can be achieved by proposed MPPT algorithm. The maximum power extracted by proposed algorithm for pattern 3 is 363.09 W and the time of tracking the MPP is 4.9 s and for pattern 4 is 301.05 W and the time of tracking the MPP is 4.6 s.
4.3 PV configuration 2S3P

The P-V characteristics of 2S3P PV configuration for shading patterns 5 and 6 exhibits two maxima, out of which only one is GMPP are shown in Fig. 10.

The 2S3P PV configuration is subjected to pattern 5 from 0 to 30s and pattern 6 from 30s. The tracking curves of proposed MPPT algorithm for shading patterns 5 and 6 of 2S3P PV configuration are presented in Fig. 11.

From Fig. 11 it is clear that MPP tracking subjected to shading pattern 5 and 6 can be achieved by proposed MPPT algorithm. The maximum power extracted by proposed algorithm for pattern 5 is 592.08 W and the time of tracking the MPP is 6.6 s and for pattern 6 is 451.57 W and the time of tracking the MPP is 6.2 s.

4.4 Performance comparison

To compare the performance of proposed WOA MPPT, GWO and PSO MPPT algorithms in terms of tracking speed and tracking efficiency subjected to all shading patterns of 6S, 3S2P and 2S3P PV configurations, results are presented in Table 2. For any MPPT algorithm both tracking efficiency and tracking time are very important to attain highest benefit from the PV system. Tracking efficiency is the ratio between maximum power tracked by algorithm to maximum power of the PV configuration (Liu et al. 2012). From Table 2, it is observed that proposed algorithm has superior tracking efficiency and tracking speed than GWO and PSO MPPT algorithms.

The performance comparison between three algorithms in terms of global maximum power extraction and tracking speeds are shown in Fig. 12 and Fig. 13.
Due to stochastic nature of the optimization algorithms, 50 trail runs were performed with the proposed and other algorithms and the statistical results are given in Table 3. From Table 3 it is noticed that the proposed algorithm has very low standard deviation compared to GWO and PSO MPPT algorithms, where as PSO MPPT suffers from LMPP trapping and leads to wastage of viable PV power.

**Table 2**
Statistical Comparison of WOA, GWO and PSO MPPT Methods

| PV configuration | Shading pattern | Tracking method | Mean best values (W) | Standard deviation (W) | Maximum power value (W) | Minimum power value (W) | Average tracking time(s) |
|------------------|-----------------|-----------------|----------------------|------------------------|-------------------------|-------------------------|-------------------------|
| 6S 1 2S3P 3S2P   |                 | WOA  | 394.5273 | 0.0000 | 394.5273 | 394.5273 | 5.4 | 99.99 |
|                  |                 | GWO  | 394.5273 | 0.0000 | 394.5273 | 394.5273 | 9.1 | 99.99 |
|                  |                 | PSO  | 394.5262 | 0.0045 | 394.5273 | 394.5087 | 12 | 99.99 |
|                  |                 | WOA  | 301.9921 | 0.0000 | 301.9921 | 301.9921 | 5.5 | 99.93 |
|                  |                 | GWO  | 301.9920 | 0.0000 | 301.9921 | 301.9854 | 8.4 | 99.93 |
|                  |                 | WOA  | 363.2528 | 0.0372 | 363.2730 | 363.1380 | 4.9 | 99.93 |
|                  |                 | GWO  | 363.1832 | 0.0894 | 363.2730 | 362.8944 | 7.8 | 99.93 |
|                  |                 | PSO  | 350.7179 | 0.2161 | 363.2730 | 207.0327 | 9.6 | 99.93 |
|                  |                 | WOA  | 300.9113 | 0.4523 | 301.0516 | 299.3440 | 4.6 | 99.93 |
|                  |                 | GWO  | 300.9214 | 0.2451 | 301.0516 | 299.3004 | 7.2 | 99.93 |
|                  |                 | PSO  | 293.8197 | 15.3695 | 301.0516 | 256.1528 | 10.8 | 99.93 |
|                  |                 | WOA  | 592.3051 | 0.0362 | 592.3128 | 592.0590 | 6.6 | 99.93 |
|                  |                 | GWO  | 592.2184 | 0.1492 | 592.3128 | 299.3004 | 10.2 | 99.93 |
|                  |                 | PSO  | 592.2854 | 0.0617 | 592.3128 | 256.1528 | 14.5 | 99.93 |
|                  |                 | WOA  | 438.7851 | 0.1050 | 438.9024 | 438.6930 | 6.2 | 99.93 |
|                  |                 | GWO  | 438.7349 | 0.0846 | 438.9024 | 438.6930 | 9.6 | 99.93 |
|                  |                 | PSO  | 352.4406 | 116.2678 | 438.9024 | 198.9040 | 13.8 | 99.93 |
5. Conclusion

In this paper a novel WOA MPPT algorithm is proposed to track GMPP of PV system subjected to Partial shading condition. The P-V characteristics of 6S, 3S2P and 2S3P configurations considering both series and shunt resistances under different partial shading conditions are presented. These characteristics exhibit multiple MPPs of which one is the GMPP and all other are LMPP. It is observed that the characteristics are highly non-linear and it is complex to track GMPP under Partial shaded condition. The proposed WOA algorithm is used to track the GMPP for above configurations and it is effective in tracking the GMPP with high accuracy and less tracking time under dynamic partial shading conditions. From results, it is seen that proposed method is superior in terms of accuracy and tracking time compared to GWO and PSO MPPT algorithms. Since the algorithms WOA, GWO and PSO are stochastic in nature, the simulations are carried for 50 trials and statistical results are presented. It is observed that the Standard Deviation (SD) of the proposed is less compared to other methods which show that the WOA is able track the GMPP effectively. But SD of PSO is very high because maximum value is trapped at local value. From results and statistical analysis, it is seen that proposed WOA MPPT algorithm proved its supremacy over GWO and PSO MPPTs.

Appendix

Parameters of PSO, GWO and WOA MPPT Algorithms

| Parameter                  | PSO | GWO | WOA |
|----------------------------|-----|-----|-----|
| Initial population (duty ratio) | Randomly between 0.1 and 0.9 | Randomly between 0.1 and 0.9 | Randomly between 0.1 and 0.9 |
| Np                         | 6   | 6   | 6   |
| Cmax                       | 2   | -   | -   |
| Cmin                       | 1   | -   | -   |
| Wmax                       | 1   | -   | -   |
| Wmax                       | 0.1 | -   | -   |
| Maximum number of iterations, kmax | 100 | 100 | 100 |
| Termination criteria       | kmax | kmax | kmax |

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