Temporal Knowledge Graph Reasoning Based on Evolutional Representation Learning

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ABSTRACT
Knowledge Graph (KG) reasoning that predicts missing facts for incomplete KGs has been widely explored. However, reasoning over Temporal KG (TKG) that predicts facts in the future is still far from resolved. The key to predict future facts is to thoroughly understand the historical facts. A TKG is actually a sequence of KGs corresponding to different timestamps, where all concurrent facts in each KG exhibit structural dependencies and temporally adjacent facts carry informative sequential patterns. To capture these properties effectively and efficiently, we propose a novel Evolutional Representation Learning network based on Graph Convolution Network (GCN), called RE-GCN, which learns the evolutional representations of entities and relations at each timestamp by modeling the KG sequence recurrently. Specifically, for the evolution unit, a relation-aware GCN is leveraged to capture the structural dependencies within the KG at each timestamp. In order to capture the sequential patterns of all facts in parallel, the historical KG sequence is modeled auto-regressively by the gate recurrent components. Moreover, the static properties of entities, such as entity types, are also incorporated via a static graph constraint component to obtain better entity representations. Fact prediction at future timestamps can then be realized based on the evolutionary entity and relation representations. Extensive experiments demonstrate that the RE-GCN model obtains substantial performance and efficiency improvement for the temporal reasoning tasks on six benchmark datasets. Especially, it achieves up to 11.46% improvement in MRR for entity prediction with up to 82 times speedup compared to the state-of-the-art baseline.

CCS CONCEPTS
\begin{itemize}
\item Computing methodologies → Temporal reasoning
\end{itemize}

KEYWORDS
Temporal knowledge graph, evolutional representation learning, graph convolution network

ACM Reference Format:
Zixuan Li\textsuperscript{1,2}, Xiaolong Jin\textsuperscript{1,2}, Wei Li\textsuperscript{3}, Saiping Guan\textsuperscript{1,2}, Jiafeng Guo\textsuperscript{1,2}, Huawei Shen\textsuperscript{1,2}, Yuanzhuo Wang\textsuperscript{1,2} and Xueqi Cheng\textsuperscript{1,2}. 2021. Temporal Knowledge Graph Reasoning Based on Evolutional Representation Learning. In Proceedings of the 44th International ACM SIGIR Conference on Research and Development in Information Retrieval (SIGIR ’21), July 11–15, 2021, Virtual Event, Canada. ACM, New York, NY, USA, 10 pages. https://doi.org/10.1145/3404835.3462963

1 INTRODUCTION
Knowledge Graphs (KGs) have facilitated many real-world applications [44]. However, they are usually incomplete, which restricts the performance and range of KG-based applications. To alleviate this problem, reasoning over KG [2, 35] that attempts to predict missing facts, is a critical task in natural language processing. Traditionally, a KG is considered to be static multi-relational data. However, recent availability of a large amount of event-based interaction data [3] that exhibits complex temporal dynamics has created the need for approaches that can characterize and reason over Temporal Knowledge Graph (TKG) [3, 11, 12]. A fact in a TKG can be represented in the form of (subject entity, relation, object entity, timestamp). Actually, a TKG can be denoted as a sequence of KGs with timestamps, each of which contains the facts that co-occur at the same timestamp. The left part of Figure 1 illustrates an example of TKG from the ICEWS18 [16] dataset. Despite the ubiquitousness of TKGs, the methods for reasoning over such kind of data are relatively unexplored both in effectiveness and efficiency.

Reasoning over a TKG from timestamps \(t_0\) to \(t_r\) primarily has two settings, interpolation and extrapolation [16]. The former [4, 9, 21] attempts to infer missing facts from \(t_0\) to \(t_r\) [16]. The latter [16, 17, 33, 34], which aims to predict future facts (events) for time \(t > t_r\), is much more challenging. For TKG, predicting new facts at future timestamps based on the observed historical KGs is helpful for understanding the hidden factors of events and responding to emerging events [20, 25, 26]. Thus, reasoning under the extrapolation setting is very vital and can be helpful for many practical applications, such as disaster relief [31] and financial analysis [1]. In this paper, the temporal reasoning tasks (i.e., reasoning under the extrapolation setting over TKGs) contains two subtasks as shown in the right part of Figure 1:
We present two subgraphs from the KGs at timestamps with the same entity and relation to each query of entity prediction and then encode the history for each query individually; (3) by characterizing TKG from the view of a KG sequence, the behaviors of Government (India) and citizen (India) on 18/01/19). To accurately predict future facts, the model is required to dive deeply into historical facts. At each timestamp, entities influence each other via concurrent facts, which form a KG and exhibit complex structural dependencies. As an example shown in Figure 1, the concurrent facts on 18/01/18 demonstrate that Government (India) is under pressure from many people, which may influence the behaviors of Government (India) on 18/01/19. Besides, the behaviors of each entity embodied in temporally adjacent facts may carry informative sequential patterns. As shown in Figure 1, the historical behaviors of N. Naidu reflect his preferences and affect his future behaviors to a certain degree. The combination of these two kinds of historical information drives the behavioral trends and preferences of entities and relations.

Some earlier attempts, including Know-evolve [33] and its extension DyRep [34], learn evolitional entity representations by modeling the occurrence of all facts in the history as a temporal point process. However, they can not model concurrent facts at the same timestamps. Some recent attempts extract related historical information for each query in a heuristic manner. Specifically, RE-NET [16, 17] extracts those directly-engaged historical facts for the given entity in each query of entity prediction and then encodes them sequentially. CyGNet [43] models the historical facts with the same entity and relation to each query of entity prediction, and thus mainly focuses on predicting facts with repetitive patterns. As a TKG is actually a KG sequence, the existing methods have three main restrictions: (1) mainly focusing on the entity and relation of a given query and neglecting the structural dependencies among all the facts in the KG at each timestamp; (2) low efficiency by encoding the history for each query individually; (3) ignoring the function of some static properties of entities such as entity types. Besides, the existing methods only focus on entity prediction, while relation prediction cannot be solved simultaneously by the same model.

In this work, we treat TKG as a KG sequence and model the whole KG sequence simultaneously to encode all historical facts into entity and relation representations to facilitate both entity and relation prediction tasks. Thus, we propose a novel GCN-based Recurrent Evolution network, namely RE-GCN, which learns the evolitional representations of entities and relations at each timestamp by modeling the KG sequence recurrently. Specifically, for each evolution unit, a relation-aware GCN is leveraged to capture the structural dependencies within the KG at each timestamp. In this way, the interactions among all the facts in a KG can be effectively modeled. The historical KG sequence is modeled auto-regressively by the gate recurrent components to capture the sequential patterns across all temporally adjacent facts efficiently. All the historical information of entities and relations in the TKG are encoded in parallel. Moreover, the static properties of entities, such as entity types, are also incorporated via a static-graph constraint component to obtain better entity representations. Then, the tasks of entity prediction and relation prediction at future timestamps can be realized based on the evolitional representations.

In general, this paper makes the following contributions:

- We propose an evolitional representation learning model RE-GCN for temporal reasoning over TKGs, which considers the structural dependencies among concurrent facts in a KG, the sequential patterns across temporally adjacent facts, and the static properties of entities. To the best of our knowledge, this is the first study that integrates all of them into the evolitional representations for temporal reasoning.
- By characterizing TKG from the view of a KG sequence, RE-GCN efficiently models all the historical information in the TKG into evolitional representations, which are applicable for both entity and relation prediction simultaneously. Therefore, it enables up to 82 times speedup compared to the state-of-the-art baseline.
- Extensive experiments demonstrate that, by modeling the history more comprehensively, RE-GCN achieves consistently and significantly better performance (up to 11.46% improvement in MRR) over both entity and relation prediction tasks on six commonly used benchmarks.

2 RELATED WORKS

Static KG Reasoning. Existing models for static KG reasoning attempt to infer missing facts in KGs. Recently, embedding based models [2, 6, 30, 35, 41] have drawn much attention. As GCN [19] is a representative model to combine content and structural features in a graph, some studies have generalized it to relation-aware GCNs so as to deal with KGs. Among them, R-GCN [28] extends GCN with relation-specific filters, and WGCN [30] utilizes learnable relation-specific weights during aggregation. VR-GCN [42] and CompGCN [36] jointly embeds both nodes and relations in a relational graph during GCN aggregation. The above models are all set in the static KG, and they cannot predict facts in the future.

Temporal KG Reasoning. Reasoning over TKG can be categorized into two settings, interpolation and extrapolation [16]. For the first setting, the models [4, 8–10, 13, 21, 27, 37, 38, 40] attempt to infer missing facts at the historical timestamps. TA-DistMult [9], TA-TransE [9] and TTransE [21] integrate the time when the facts
work to model the frequency of the historical facts with the same tamp and the static properties of entities. Differently, RE-GCN of 1-hop subgraphs related to the given subject entity. They both of each given query, which encodes the historical facts related to all the events have the summary text in the practical application. summary into the modeling of future fact prediction. However, not Glean [5] incorporates a word graph constructed by the event temporal point process. They are more capable of modeling TKGs to predict new facts at future timestamps based on historical ones. The extrapolation setting, which this paper focuses on, attempts the prediction of the facts at a future timestamp \( t + 1 \) depends on the KGs at the latest \( m \) timestamps (i.e., \( \{G_1, \ldots, G_m\} \)) and the information of the historical KG sequence is modeled in the evolutionary embedding matrices of the entities \( H \in \mathbb{R}^{d \times |V|} \) and the relations \( R \in \mathbb{R}^{d \times |R|} \) at timestamp \( t \) (\( d \) is the dimension of the embeddings), the two temporal reasoning tasks can be formulated as follows:

**Task 1. Entity Prediction.** Given a query \( (s, r, ?, t + 1) \), RE-GCN models the conditional probability vector of all object entities with the subject entity \( s \), the relation \( r \) and the historical KG sequence \( G_{t-m+1:t} \) given:

\[
\tilde{p}(o|s, r, G_{t-m+1:t}) = \tilde{p}(o|s, r, H_r).
\]

**Task 2. Relation Prediction.** Given a query \( (s, ?, o, t + 1) \), RE-GCN models the conditional probability vector of all relations with the subject entity \( s \), the object entity \( o \) and the historical KG sequence \( G_{t-m+1:t} \) given:

\[
\tilde{p}(r|s, o, G_{t-m+1:t}) = \tilde{p}(r|s, o, H_r).
\]

### 4 THE RE-GCN MODEL

RE-GCN integrates the structural dependencies in a KG at each timestamp, the informative sequential patterns across temporally adjacent facts, and the static properties of entities into the evolutionary representations of entities and relations. Based on the learned entity and relation representations, temporal reasoning at future
timesteps can be made with various score functions. Thus RE-GCN contains an evolution unit and multi-task score functions, as illustrated in Figure 2. The former is employed to encode the historical KG sequence and obtain the evolutional representations of entities and relations. The latter contains score functions for corresponding tasks with the evolutional representations (i.e., embeddings) at the final timestamp as the input.

4.1 The Evolution Unit

The evolution unit consists of a relation-aware GCN, two gate recurrent components, and a static graph constraint component. The relation-aware GCN attempts to capture the structural dependencies within the KG at each timestamp. The two gate recurrent components model the historical KG sequence auto-regressively. Specifically, a time gate recurrent component and a GRU component get the evolutional representations of entities and relations at each timestamp correspondingly. The static graph constraint component integrates the static properties to the evolutional embeddings by adding some constraints between static embeddings and evolutional embeddings of entities. Formally, the evolution unit computes a mapping from a sequence of KGs at the latest \( m \) timesteps (i.e., \( \{G_t, m+1, ... , G_t\} \)) to a sequence of entity embedding matrices (i.e., \( \{H_t, m+1, ... , H_t\} \)) and a sequence of relation embedding matrices (i.e., \( \{R_t, m+1, ... , R_t\} \)) recurrently. Particularly, the input at the first timestamp, including the entity embedding matrix \( \mathbf{H} \) and the relation embedding matrix \( \mathbf{R} \), are randomly initialized.

4.1.1 Structural Dependencies among Concurrent Facts. The structural dependencies among concurrent facts capture the associations among the entities through facts and the associations among relations through the shared entities. Since each KG is a multi-relational graph and GCN is a powerful model for the graph-structured data [28, 30, 36, 42], an \( \omega \)-layer relation-aware GCN is used to model the structural dependencies. More specifically, for a KG at timestamp \( t \), an object entity \( o \) at layer \( l \in [0, \omega - 1] \) gets information from its subject entities under a message-passing framework with embeddings of the relations at layer \( l \) considered and obtains its embedding at the next \( l + 1 \) layer, i.e.,

\[
\mathbf{r}^t_{o, l+1} = f \left( \frac{1}{\mathbf{c}_0} \sum_{(s,r,o)\in E_t} \mathbf{W}^t_3 \left( \mathbf{r}^t_{s, l} + \mathbf{r}_t \right) + \mathbf{W}^t_2 \mathbf{r}^t_{o, l} \right),
\]

where \( \mathbf{r}^t_{o, l}, \mathbf{r}^t_{s, l}, \mathbf{r}_t \) denote the \( l \)th layer embeddings of entities \( o, s \) and relation \( r \) at timestamp \( t \), respectively; \( \mathbf{W}^t_3, \mathbf{W}^t_2 \) are the parameters for aggregating features and self-loop in the \( l \)th layer; \( \mathbf{r}^t_{s, l} + \mathbf{r}_t \) implies the translational property between the subject entity and the corresponding object entity via the relation \( r \); \( \mathbf{c}_0 \) is a normalization constant, equal to the in-degree of entity \( o \); \( f(\cdot) \) is the ReLU activation function [39]. Note that, for those entities that are not involved in any fact, only a self-loop operation with the extra parameters \( \mathbf{W}^t_3 \) is carried out. Actually, the relation-aware GCN gets the entity embeddings according to the facts occurred among them at each timestamp and the self-loop operation can be considered as the self-evolution of the entities.

4.1.2 Sequential Patterns across Temporally Adjacent Facts. For an entity \( o \), the sequential patterns contained in its historical facts reflect its behavioral trends and preferences. To cover the historical facts as many as possible, the model needs to take all its temporally adjacent facts into consideration. As the output of the final layer of the relation-aware GCN, \( \mathbf{h}^{t+1}_{o, t-1} \) already models the structure of the adjacent facts at timestamp \( t - 1 \), one straightforward and effective approach to contain the information of the temporally adjacent facts is to use the output entity embedding matrix at \( t - 1 \), \( \mathbf{H}_{t-1} \), as the input of the relation-aware GCN at \( t \), \( \mathbf{H}^t \). Therefore, the potential sequential patterns are modeled by stacking the \( \omega \)-layer relation-aware GCN. However, although the adjacent KGs are different, the over-smoothing problem [19], i.e., the embeddings of entities converge to the same values, also exists when the repetitive relations occur between the same entity pairs at adjacent timestamps [43]. And when the historical KG sequence gets longer, the large number of stacked layers of GCN may cause the vanishing gradient problem. Thus, following [23], we apply a time gate recurrent component to alleviate these problems. In this way, the entity embedding matrix \( \mathbf{H}_t \) is determined by two parts, namely, the output \( \mathbf{H}^t \) of the final layer of the relation-aware GCN at timestamp \( t \) and \( \mathbf{H}_{t-1} \) from the previous timestamp. Formally,

\[
\mathbf{H}_t = \mathbf{U}_t \odot \mathbf{H}^t + (1 - \mathbf{U}_t) \odot \mathbf{H}_{t-1},
\]

where \( \odot \) denotes the dot product operation. The time gate \( \mathbf{U}_t \in \mathbb{R}^{d \times d} \) conducts nonlinear transformation as:

\[
\mathbf{U}_t = \sigma(\mathbf{W}_4 \mathbf{H}_{t-1} + b),
\]

where \( \sigma(\cdot) \) is the sigmoid function and \( \mathbf{W}_4 \in \mathbb{R}^{d \times d} \) is the weight matrix of the time gate. Besides, the sequential pattern of relations captures the information of entities involved in the corresponding facts. Thus, the embeddings of a relation \( \mathbf{r}_t \) at timestamp \( t \) is influenced by the evolutional embeddings of \( r \)-related entities \( \mathcal{V}_{r,t} = \{i(i, r, o, t) \text{ or } (s, r, i, t) \in E_t \} \) at timestamp \( t \) and its own embedding at timestamp \( t - 1 \). Thus, a GRU component is adopted to model the sequential pattern of relations.

By applying mean pooling operation over the embedding matrix of \( r \)-related entities at timestamp \( t - 1 \), \( \mathbf{H}_{t-1, \mathcal{V}_{r,t}} \), the input of the GRU at timestamp \( t \) for relation \( r \), is

\[
\mathbf{r}^t_r = [pooling(\mathbf{H}_{t-1, \mathcal{V}_{r,t}}); \mathbf{r}_t],
\]

where \( \mathbf{r}^t_r \) is the embedding of relation \( r \) in \( \mathbf{R} \) and \( [; ;] \) denotes the vector concatenation operation. For the relation that does not have corresponding facts occurred at timestamp \( t \), \( r^t_r = 0 \). Then we update the relation embedding matrix \( \mathbf{R}_{t-1} \) to \( \mathbf{R}_t \) via the GRU,

\[
\mathbf{R}_t = \text{GRU}(\mathbf{R}_{t-1}, \mathbf{r}^t_r),
\]

where \( \mathbf{R}^t_r \in \mathbb{R}^{d \times d} \) consists of \( \mathbf{r}^t_r \) of all the relations. Note that, the L2-norm of each line of \( \mathbf{H}_t \) and \( \mathbf{R}_t \) is constrained to 1.

4.1.3 Static Properties. Besides the information contained in the historical KG sequence, some static properties of entities, which form a static graph, can be seen as the background knowledge of the TKG and is helpful for the model to learn more accurate evolutional representations of entities. Thus we incorporate the static graph into the modeling of the evolutional representations. We construct the static graphs of the three TKGs from ICEWS based on the entity property information originally contained in the name strings of entities. Most name strings of entities therein
are in the form of ‘entity types (country)’. Take an entity named ‘Police (Australia)’ in ICEWS18 [17] for example, we add relation ‘isA’ from this entity to the property entity ‘Police’ and relation ‘country’ to the property entity ‘Australia’. The bottom left of figure 2 shows an example of a static graph. Since the static graph is a multi-relational graph and R-GCN [28] can model the multi-relational graph without any more extra embeddings for relations. Thus, we adopt a 1-layer R-GCN [28] without self-loop to get the static embeddings of entities in the TKG. Then, the update rule for the static graph is defined as follows:

\[
\hat{h}^s_i = \gamma \left( \frac{1}{c_i} \sum_{(r,s,j) \in E^s} W_r \hat{h}^s_j (j) \right),
\]

where \(\hat{h}^s_i\) and \(\hat{h}^s_j\) are the \(i^{th}\) and \(j^{th}\) lines of \(H^s\) and \(H^s\), which are the output and randomly initialized input embedding matrices, respectively; \(W_r \in \mathbb{R}^{d \times d}\) is the relation matrix of \(r^s\) in R-GCN; \(\gamma(\cdot)\) is ReLU function; \(c_i\) is a normalization constant equal to the number of entities connected with entity \(i\). Note that, \(|\hat{h}^s_i|_2 = 1\).

To reflect the static properties in the learned sequence of entity embedding matrices \(H_{r-m}, H_{r-m+1}...H_{r}\), we confine the angle between the evolutionary embedding and the static embedding of the same entity not to exceed a timestamp-related threshold. It increases over time since the permitted variable range of the evolutionary embeddings of entities continuously extends over time with more and more facts occurring. Thus, it is defined as

\[
\theta_x = \min(y, 90^\circ),
\]

where \(y\) denotes the ascending pace of the angle and \(x \in [0, 1, ..., m]\). We set the max angle of the two embeddings of an entity to 90\(^\circ\).

Then, the cosine value of the angle between the two embeddings of entity \(i\), denoted as \(\cos(\hat{h}^s_i, \hat{h}_{t-m+i})\), should be more than \(\cos(\theta_x)\).

Thus, the loss of the static graph constraint component at timestamp \(t\) can be defined as below:

\[
L_{x}^s = \sum_{i=0}^{\left|E^s\right|-1} \max\{\cos(\theta_x - \cos(\hat{h}^s_i, \hat{h}_{t-m+i}), 0)\}.
\]

The loss of the static graph constraint component is \(L_x^s = \sum_{x=0}^{m} L_x^s\).

### 4.2 Score Functions for Different Tasks

Previous works [6, 30, 36] on KG reasoning involve score functions (i.e., decoder) to model the conditional probability in Equation (1) and (2), which can be seen as the probability score of candidate triples \((s, r, o)\). As the previous work [36] shows that GCN with the convolutional score functions gets good performance on KG reasoning and in order to reflect the translational property of the evolutionary embeddings of entities and relations implied in Equation (3), we choose ConvTransE [30] as our decoder. ConvTransE contains a one-dimensional convolution layer and a fully connected layer. We use ConvTransE \((\cdot)\) to represent these two layers. Then, the probability vector of all entities is:

\[
\hat{p}(o | s, r, H_r, R_t) = \sigma(H_o \text{ConvTransE}(\hat{s}_i, \hat{r}_j)).
\]

Similarly, the probability vector of all the relations is:

\[
\hat{p}(r | s, o, H_r, R_t) = \sigma(R_r \text{ConvTransE}(\hat{s}_i, \hat{r}_j)),
\]

where \(\sigma(\cdot)\) is the sigmoid function, \(\hat{s}_i, \hat{r}_i, \hat{a}_i\) are the embeddings of \(s, r\) and \(o\) in \(H_r\) and \(R_t\), respectively. ConvTransE \((\hat{s}_i, \hat{r}_j)\) and ConvTransE \((\hat{s}_i, \hat{a}_j)\) \(\in \mathbb{R}^{d \times 1}\). The details of ConvTransE are omitted for brevity. Note that, ConvTransE can be replaced by other score functions.

### 4.3 Parameter Learning

Both the entity prediction task and the relation prediction task can be seen as the multi-label learning problems. Let \(\hat{y}_{t+1}^e \in \mathbb{R}^{|V|}\) and \(\hat{y}_{t+1}^r \in \mathbb{R}^{|R|}\) denote the label vectors for the two tasks at the timestamp \(t + 1\), respectively. The elements of vectors \(\hat{y}_{t+1}^e \in \mathbb{R}^{|V|}\) and \(\hat{y}_{t+1}^r \in \mathbb{R}^{|R|}\) are 1 for facts that do occur, otherwise, 0. Then,

\[
\begin{align*}
L^e &= \sum_{i=0}^{T-1} \sum_{(s, r, o, t+i) \in E_{t+i}} \sum_{j=0}^{\left|V^s\right|-1} \hat{y}_{t+1,i}^e \log p_i(o | s, r, H_r, R_t), \\
L^r &= \sum_{i=0}^{T-1} \sum_{(s, r, o, t+i) \in E_{t+i}} \sum_{j=0}^{\left|R^r\right|-1} \hat{y}_{t+1,i}^r \log p_i(r | s, o, H_r, R_t).
\end{align*}
\]

where \(T\) is the number of timestamps in the training set. \(\hat{y}_{t+1,i}^e, \hat{y}_{t+1,i}^r\) is the \(i_{th}\) element in \(\hat{y}_{t+1}^e, \hat{y}_{t+1}^r\). \(p_i(o | s, r, H_r, R_t)\) and \(p_i(r | s, o, H_r, R_t)\) are the probability score of entity \(i\) and relation \(i\).

The two temporal reasoning tasks are conducted under the multi-task learning framework. Therefore, the final loss \(L = \lambda_1 L^e + \lambda_2 L^r + L^s\). \(\lambda_1\) and \(\lambda_2\) are the parameters that control the loss terms.

### 4.4 Computational Complexity Analysis

To see the efficiency of the proposed RE-GCN, we analyze the computational complexity of its evolution unit. The time complexity of the relation-aware GCN at a timestamp \(t\) is \(O(|E| \omega)\), where \(|E|\) is the maximum number of concurrent facts in the historical KG sequence. The pooling operation to get the input of the GRU component and the relation-aware GCN, the time complexity for the evolution unit is finally \(O(m(|E| \omega + |R| |D| + |E|^s))\).

### 5 EXPERIMENTS

#### 5.1 Experimental Setup

**5.1.1 Datasets.** There are six typical TKGs commonly used in previous works, namely, ICEWS18 [16], ICEWS14 [9], ICEWS05-15 [9], WIKI [21], YAGO [24] and GDELT [22]. The first three ones are from the Integrated Crisis Early Warning System [3] (ICEWS). GDELT [16] is from the Global Database of Events, Language, and Tone [22]. We evaluate RE-GCN on all these datasets. We divide ICEWS14 and ICEWS05-15 into training, validation, and test sets, with a proportion of 80%, 10% and 10% by timestamps following [16]. The details of the datasets are presented in Table 2. The time interval represents time granularity between temporally adjacent facts.

**5.1.2 Evaluation Metrics.** In the experiments, MRR and Hits@1, 3, 10 are employed as the metrics for entity prediction and relation prediction. For the entity prediction task on WIKI and YAGO, we only report the MRR and Hits@3 results because the results of Hits@1 were not reported by the prior work RE-NET [16].
As mentioned in [7, 14, 15], the filtered setting used in [2, 16, 43], which removes all the valid facts that appear in the training, validation, or test sets from the ranking list of corrupted facts, is not suitable for temporal reasoning tasks. Take a typical query \((s, r, ?, t_1)\) with answer \(o_1\) in the test set for example, and assume there is another fact \((s, r, o_2, t_2)\). Under this filtered setting, \(o_2\) will be wrongly considered a correct answer and thus removed from the ranking list of candidate answers. However, \(o_2\) is incorrect for the given query, as \((s, r, o_2)\) occurs at timestamp \(t_2\) instead of \(t_1\). Thus, the filtered setting may possibly get incorrect higher ranking scores. Without loss of generality, only the experimental results under the raw setting are reported.

5.1.3 Baselines. The RE-GCN model is compared with static KG reasoning models and TKG reasoning models. DistMult [41], ComplEx [35], R-GCN [28], ConvE [6], ConvTransE [30], RoteE [32] are selected as static models. HyTE [4], TTransE [21] and TA-DistMult [9] are selected as the temporal models under the interpolation setting. For temporal models under the extrapolation setting, CyGNet [43] and RE-NET [16] are compared. For Know-evolve and Mult [9] are selected as the temporal models under the interpolation setting. For temporal models under the extrapolation setting, i.e., those in the second blocks of Tables 3 and 4 because RE-GCN additionally captures temporally sequential patterns and static properties of entities. It can thus obtain more accurate evolutional representations for the unobserved timestamps. Especially, RE-GCN outperforms the temporal models for the extrapolation setting (i.e., those in the third blocks of Tables 3 and 4). It outperforms RGCRN because the newly designed graph convolution operation and the two recurrent components in the evolution unit learn better evolutional embeddings and the static graph helps learn better evolutional embeddings of entities. CyGNet and RE-NET’s good performance verify the importance of the repetitive patterns and 1-hop neighbors to the entity prediction task. Despite this, it is not surprising that RE-GCN performs better than CyGNet because there is much useful information except the repetitive patterns in the history. RE-GCN also performs better than RE-NET, which neglects the structural dependencies within a KG and the static properties of entities. By capturing more comprehensive structural dependencies and sequential patterns, RE-GCN outperforms RE-NET on most datasets. From the last two lines in Tables 3 and 4, it can be observed that the performance gap between the last two lines becomes large when the time interval between two adjacent timestamps of the datasets becomes large. For the two datasets, WIKI and YAGO, with the time interval as one year, the model’s performance drops rapidly without knowing the ground truth history. This is because the evolutionary representations become inaccurate when the time interval is large during the multi-step inference.

Note that RE-GCN even achieves the improvements of 8.97/11.46% in MRR, 10.60/12.91% in Hits@3 and 12.61/14.01% in Hits@10 based on the observations in the training set, we evaluate the performance of RE-GCN with the evolutional embeddings at the final timestamp of the training set as the input of score functions following [43]. Besides, we also report the results of the models with ground truth history given during multi-step inference on the test set, namely, GT. All experiments are carried out on Tesla V100. Codes are available at https://github.com/Lee-zix/RE-GCN.

5.2 Experimental Results

5.2.1 Results on Entity Prediction. The experimental results on the entity prediction task are presented in Tables 3 and 4. RE-GCN consistently outperforms the baselines on the three ICEWS datasets, WIKI and YAGO. The results convincingly verify its effectiveness. Specifically, RE-GCN significantly outperforms the static models (i.e., those in the first blocks of Tables 3 and 4) because RE-GCN considers the sequential patterns across timestamps. RE-GCN performs better than the temporal models for the interpolation setting (i.e., those in the second blocks of Tables 3 and 4) because RE-GCN additionally captures temporally sequential patterns and static properties of entities. It can thus obtain more accurate evolutional representations for the unobserved timestamps.

| Datasets      | | | | | | Time interval |
|---------------|---------------|---------------|---------------|---------------|---------------|----------------|
| ICEWS18       | 23,033        | 256           | 373,018       | 45,995        | 49545         | 29,774         | 8,647          | 24 hours       |
| ICEWS14       | 6,869         | 230           | 74,845        | 8,514         | 7,371         | 8,442          | 3,499          | 24 hours       |
| ICEWS05-15    | 10,094        | 251           | 368,868       | 46,302        | 46,159        | 12,392         | 5,179          | 24 hours       |
| WIKI          | 12,554        | 24            | 539,286       | 67,538        | 63,110        | –              | –              | 1 year         |
| YAGO          | 10,623        | 10            | 161,540       | 19,523        | 20,026        | –              | –              | 1 year         |
| GDELT         | 7,691         | 240           | 1,734,399     | 238,765       | 305,241       | –              | –              | 15 mins        |

Table 2: Statistics of the datasets (|\(E_{\text{train}}\)|, |\(E_{\text{valid}}\)|, |\(E_{\text{test}}\)| are the numbers of facts in training, validation, and test sets.)
Table 3: Performance (in percentage) for the entity prediction task on ICEWS18, ICESW14 and ICEWS05-15 with raw metrics.

| Model     | ICE18     | ICE14     | ICE05-15  |
|-----------|-----------|-----------|-----------|
|           | MRR  | H@1 | H@3 | H@10 | MRR  | H@1 | H@3 | H@10 | MRR  | H@1 | H@3 | H@10 |
| DistMult  | 13.86 | 5.61 | 15.22 | 31.26 | 20.32 | 6.13 | 27.59 | 46.61 | 19.91 | 5.63 | 27.22 | 47.33 |
| ComplEx   | 15.45 | 8.04 | 17.19 | 30.73 | 22.61 | 9.88 | 28.93 | 47.57 | 20.26 | 6.66 | 26.43 | 47.31 |
| R-GCN     | 15.05 | 8.13 | 16.49 | 29.00 | 28.03 | 19.42 | 34.42 | 47.89 | 27.13 | 18.83 | 30.41 | 43.16 |
| ConvE     | 22.81 | 13.63 | 25.83 | 41.43 | 30.30 | 21.30 | 34.98 | 50.03 | 30.28 | 20.79 | 33.80 | 49.95 |
| RotatE    | 14.53 | 6.47 | 15.78 | 31.86 | 31.50 | 22.46 | 34.98 | 50.03 | 20.79 | 10.42 | 21.35 | 36.92 |
| HyTE      | 7.41  | 3.10 | 7.33  | 16.01 | 16.78 | 6.13 | 27.59 | 46.61 | 16.05 | 6.53 | 21.35 | 34.72 |
| TTransE   | 8.44  | 1.85 | 8.95  | 22.38 | 12.86 | 3.14 | 15.72 | 33.65 | 16.53 | 5.51 | 20.77 | 39.26 |
| TA-DistMult | 16.42 | 8.60 | 18.13 | 32.51 | 26.22 | 16.83 | 29.72 | 45.23 | 27.51 | 17.57 | 31.46 | 47.32 |
| RGCN      | 23.46 | 14.24 | 26.62 | 41.96 | 33.31 | 24.08 | 36.55 | 51.54 | 35.93 | 26.23 | 40.02 | 54.63 |
| CyGNet    | 24.98 | 15.54 | 28.58 | 43.54 | 34.68 | 25.35 | 38.88 | 53.16 | 28.93 | 18.23 | 31.50 | 47.31 |
| RE-NET    | 26.17 | 16.43 | 29.89 | 44.37 | 35.77 | 25.99 | 40.10 | 54.87 | 30.28 | 20.79 | 33.80 | 49.95 |
| RE-GCN    | 27.51 | 17.82 | 31.17 | 46.55 | 37.78 | 27.17 | 42.50 | 58.84 | 38.27 | 27.43 | 43.06 | 59.93 |
| RE-GCN w. GT | 30.55 | 20.00 | 34.73 | 51.46 | 41.50 | 30.86 | 46.60 | 62.47 | 46.41 | 35.17 | 52.76 | 67.64 |

Table 4: Performance (in percentage) for the entity prediction task on WIKI, YAGO and GDELT with raw metrics.

| Model     | WIKI     | YAGO     | GDELT    |
|-----------|----------|----------|----------|
|           | MRR  | H@3 | H@10 | MRR  | H@3 | H@10 | MRR  | H@1 | H@3 | H@10 |
| DistMult  | 27.96 | 32.45 | 39.51 | 44.05 | 49.70 | 59.94 | 8.61 | 3.91 | 8.27 | 17.04 |
| ComplEx   | 27.69 | 31.99 | 38.61 | 44.09 | 49.57 | 59.64 | 9.84 | 5.17 | 9.58 | 18.23 |
| R-GCN     | 13.96 | 15.75 | 22.05 | 20.25 | 24.01 | 37.30 | 12.17 | 7.40 | 12.37 | 20.63 |
| ConvE     | 26.03 | 30.51 | 39.18 | 41.22 | 47.03 | 59.90 | 18.37 | 11.13 | 19.11 | 31.50 |
| RotatE    | 30.89 | 34.30 | 41.45 | 46.67 | 52.22 | 62.52 | 19.07 | 11.85 | 20.32 | 33.14 |
| HyTE      | 25.40 | 29.16 | 37.54 | 34.42 | 39.73 | 46.98 | 6.69 | 0.01 | 7.57 | 19.06 |
| TTransE   | 20.66 | 23.88 | 33.04 | 26.10 | 36.28 | 47.73 | 5.53 | 0.46 | 4.97 | 15.37 |
| TA-DistMult | 26.44 | 31.36 | 38.51 | 42.08 | 46.77 | 59.39 | 3.62 | 0.52 | 2.26 | 8.37 |
| RGCN      | 23.46 | 31.44 | 38.58 | 43.71 | 48.53 | 56.98 | 18.63 | 11.29 | 19.80 | 32.42 |
| CyGNet    | 30.77 | 33.83 | 41.19 | 46.72 | 52.48 | 61.52 | 18.05 | 11.13 | 19.11 | 31.50 |
| RE-NET    | 30.87 | 33.55 | 41.27 | 46.81 | 52.71 | 61.93 | 19.60 | 12.03 | 20.56 | 33.89 |
| RE-GCN    | 39.84 | 44.43 | 53.88 | 58.27 | 65.62 | 75.94 | 19.15 | 11.92 | 20.40 | 33.19 |
| RE-GCN w. GT | 51.53 | 58.29 | 69.53 | 63.07 | 71.17 | 82.07 | 19.31 | 11.99 | 20.61 | 33.59 |

Table 5: Performance on the relation prediction task.

 over the best baseline on WIKI and YAGO. For the two datasets, there are more structural dependencies at each timestamp because the time interval is much larger than the other datasets. Therefore, only modeling repetitive patterns or one-hop neighbors will lose a lot of structural dependencies and sequential patterns. The results demonstrate that RE-GCN is more capable of modeling these datasets containing complex structural dependencies among concurrent facts.

The experimental results of static models and temporal models are similarly poor on GDELT, as compared with those of the other five datasets. We further analyze the GDELT dataset and find that many of its entities are abstract concepts that do not indicate specific entities (e.g., POLICE and GOVERNMENT). Among the top 50 frequent entities, 28 are abstract concepts and 43.72% corresponding facts involve abstract concepts. Those abstract concepts make the temporal reasoning for some entities under the raw setting almost impossible, since we cannot predict a government’s activities without knowing which country it belongs to. Thus, all the models can only predict partial facts in the GDELT dataset and get similar results. Besides, the noise produced by the abstract concepts influences the evolutional representations of other entities as RE-GCN
models the KG sequence as a whole, which makes the results of RE-GCN a little worse than RE-NET.

### 5.2.2 Results on Relation Prediction

Since some models are not designed for the relation prediction task and for space limitation, we select the typical ones from the baselines and present the experimental results in terms of only MRR in Table 5. In more detail, we select ConvE [6], ConvTransE [30] from the static models, as well as RGCRN [29] from the temporal models. RE-NET and CyGNet are not adopted, as they cannot be applied to the relation prediction task directly. It can observe that RE-GCN performs better than all the baselines. The outperformance of RE-GCN demonstrates that our evolution unit can obtain more accurate evolutionary representations by modeling the history comprehensively.

The performance gap between RE-GCN and other baselines on the relation prediction task is smaller than the entity prediction task. It is because the number of relations is much less than the number of entities. Fewer candidates make the relation prediction task much easier than the entity prediction task. The performance on WIKI and YAGO is much better than the other datasets because the numbers of relations in the two datasets are only 24 and 10, respectively. The results on the GDELT dataset for the static models and the temporal models are also similarly poor, which verifies our observations mentioned in Section 5.2.1 again.

### 5.3 Comparison on Prediction Time

To further verify the effectiveness of our evolution unit under different score functions, we replace the ConvTransE in RE-GCN with a one layer Fully Connected Network (FCN), denoted as +FCN w. GT. The experimental results are presented in Tables 6 and 7. It can be observed that the results are worse than RE-GCN w. GT on most datasets. It matches the observation in [42], the convolutional score functions are more suitable for the GCN. However, even with a simple score function, +FCN w. GT still shows strong performance on both entity and relation predictions.

### 5.4 Ablation Studies

#### 5.4.1 Impact of the Evolution Unit

To demonstrate how the evolution unit contributes to the final results of RE-GCN, we conduct experiments of only using the ConvTransE score function with the randomly initialized learnable embeddings. The results denoted as -EE w. GT, are demonstrated in Tables 6 and 7. It can be observed that removing the evolution unit has a great impact on the results for all the datasets except GDELT, suggesting that modeling the historical information is vital for all the datasets. For GDELT, only using the ConvTransE can get good results. It also matches our observations mentioned in Section 5.2.1.

To further verify the effectiveness of our evolution unit under different score functions, we replace the ConvTransE in RE-GCN with a one layer Fully Connected Network (FCN), denoted as +FCN w. GT. The experimental results are presented in Tables 6 and 7. It can be observed that the results are worse than RE-GCN w. GT on most datasets. It matches the observation in [42], the convolutional score functions are more suitable for the GCN. However, even with a simple score function, +FCN w. GT still shows strong performance on both entity and relation predictions.

#### 5.4.2 Impact of the Static Graph Constraint Component

The results denoted as –st w. GT in Tables 6 and 7 demonstrate the performance of RE-GCN without the static graph constraint component. It can be seen that –st w. GT performs consistently worse than RE-GCN w. GT in ICEWS datasets, which justifies the necessity of the static graph constraint component to the RE-GCN model. The static information can be seen as the background knowledge of the TKG. The entity type and location information in the static graph enriches the evolutionary representations of entities and helps obtain better initial evolutionary representations of entities. Note that, even without the static information, –st w. GT still outperforms the state-of-art RE-NET w. GT and RGCRN w. GT.

#### 5.4.3 Impact of the Time Gate Recurrent Component

The results denoted as –tg w. GT in Tables 6 and 7 denote the variants of RE-GCN directly using the evolutionary representations at the last timestamp as the input of the evolution unit at the current timestamp without the time gate. The performance of –tg w. GT decreases rapidly when the historical KG sequence gets longer, as compared to RE-GCN w. GT, which sufficiently indicates the necessity of the time gate recurrent component.

### Table 6: Ablation studies on entity prediction.

| Model     | ICE18 | ICE14 | ICE05-15 | WIKI | YAGO | GDELT |
|-----------|-------|-------|----------|------|------|-------|
| RE-GCN w. GT | 30.55 | 41.50 | 46.41    | 51.53 | 63.07 | 19.31 |
| RE-NET w. GT | 27.87 | 39.13 | 42.92    | 32.44 | 48.60 | 21.29 |
| -EE w. GT  | 23.22 | 31.50 | 30.28    | 30.89 | 46.67 | 19.07 |
| +FCN w. GT | 29.32 | 40.34 | 45.89    | 46.00 | 58.96 | 19.02 |
| -st w. GT  | 29.10 | 39.48 | 44.68    | -     | -    | -     |
| -tg w. GT  | 24.51 | 34.85 | 37.65    | 51.70 | 62.23 | 18.55 |

### Table 7: Ablation studies on relation prediction.

| Model     | ICE18 | ICE14 | ICE05-15 | WIKI | YAGO | GDELT |
|-----------|-------|-------|----------|------|------|-------|
| RE-GCN w. GT | 40.53 | 41.06 | 40.63    | 97.92 | 97.74 | 19.22 |
| RGCRN w. GT  | 38.07 | 38.28 | 39.33    | 90.12 | 91.27 | 18.73 |
| -EE w. GT  | 38.00 | 38.40 | 38.26    | 86.64 | 90.98 | 18.97 |
| +FCN w. GT | 39.63 | 40.23 | 40.55    | 97.23 | 93.66 | 19.03 |
| -st w. GT  | 39.23 | 40.00 | 40.38    | -     | -    | -     |
| -tg w. GT  | 37.47 | 38.14 | 37.62    | 97.56 | 93.86 | 18.94 |
Table 8: Case study. The first two lines are two cases for entity prediction and the last line is a case for relation prediction.

| Subsets | Tasks | Entity Prediction | Relation Prediction |
|---------|-------|-------------------|---------------------|
|         |       | seen | unseen | seen | unseen |
|         |       | a    | b     | c     | d     | e     | a    | b    | c     | d     | e     |
|         | Subsets | % |        |        |        |        |        |        |        |        |        |        |
|         | H@3   | 0   | 1.8   | 3.9   | 13.8  | 21.0  | 19.8  | 7.6   | 9.1   | 9.8   | 13.2  | 0     | 22.3  | 6.0   | 5.2   | 1.0   | 37.3  | 8.7   | 11.4  | 5.2   | 1.0   |

Table 9: Hits@3 on different subsets from the validation set of ICEWS18. The % row shows the proportion of each subset.

5.5 Case Study

In order to show the structural dependencies among concurrent facts and the sequential patterns across temporally adjacent facts learned by RE-GCN, we illustrate in Table 9 three cases from the test set of ICEWS18 where RE-GCN ranks the right answers at the top. The first case shows the sequential pattern that \((A, \text{host a visit}, B, t=2)\) can lead to \((A, \text{diplomatic cooperation}, B, t)\). The second case shows that the sequential pattern \((A, \text{Conduct bombing}, B, t=2), (B, \text{Make statement}, C, t=1)\) and structural dependencies of \(C\) at timestamp \(t=1\) joint lead to the final result. The third case illustrates the sequential pattern \((A, \text{Demonstrate}, B, t=2), (B, \text{Endorse}, C, t=1)\) helps the relation prediction \((A, \text{Defense ministry}, B, t)\). By modeling the KG sequence as a whole, RE-GCN does not omit useful information in the history.

5.6 Detailed Analysis

In order to get insight into the performance of RE-GCN on different kinds of data, we conduct a detailed analysis on the validation set of ICEWS18. For entity prediction, we split the validation set according to the number of the one-hop neighbors of a given entity (0 (a), 1 (b), 2-3 (c), 4-10 (d), >10 (e)) and whether the answer entity has direct interactions with the given entity (i.e., seen and unseen) at the latest \(m (m=6)\) timestamps. For relation prediction, we split the validation set according to the number of relations between two given entities (0 (a), 1 (b), 2-3 (c), 4-10 (d), >10 (e)) and whether the answer relation occurred between the given entities at the latest \(m\) timestamps. (i.e., seen and unseen). Table 9 shows the results of RE-GCN with Hits@3 on each subset. For entity prediction, it can be observed that the performance decreases when the number of the neighbors gets large and RE-GCN gets better results in the subset where the two entities have seen each other in the history. Interestingly, RE-GCN can even conduct predictions where the subject entities have no history. A possible reason is that the static graph and the shared initial evolutional representations already provide some background knowledge and information out of the historical KG sequence. For relation prediction, it can be seen that the performance decreases when the number of relations is large. Table 9 also demonstrates the repetitive facts account for a certain proportion in the dataset, which further proves the necessity of the time gate recurrent component in RE-GCN.

6 CONCLUSIONS

This paper proposed RE-GCN for temporal knowledge graph reasoning, which learns evolutional representations of entities and relations by capturing the structural dependencies among concurrent facts and the informative sequential patterns across temporally adjacent facts. Moreover, it incorporates the static properties of entities such as entity types into the evolutional representations. Thus, temporal reasoning is conducted with various score functions based on the evolutional representations at the final timestamps. Experimental results on six benchmarks demonstrate the significant merits and superiority of RE-GCN on two temporal reasoning tasks. Moreover, by modeling the KG sequence as a whole, RE-GCN enables 17 to 82 times speedup in entity prediction comparing to RE-NET, the state-of-the-art baseline.

ACKNOWLEDGE

The work is supported by the National Key Research and Development Program of China under grant 2016YFB1000902, the National Natural Science Foundation of China under grants U1911401, 62002341, 61772501, U1836206, 91646120, and 61722211, the GFKJ Innovation Program, Beijing Academy of Artificial Intelligence under grant BAAI2019ZD0306, and the Lenovo-CAS Joint Lab Youth Scientist Project.
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