Stacking faults in $\alpha$-RuCl$_3$ revealed by local electric polarization

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We present out-of-plane dielectric and magnetodielectric measurements of single crystalline $\alpha$-RuCl$_3$ with various degrees of stacking faults. A frequency dependent, but field independent, dielectric anomaly appears at $T_A (f = 100\text{kHz}) \sim 4$ K once both magnetic transitions at $T_{N1} \sim 7$ K and $T_{N2} \sim 14$ K set in. The observed dielectric anomaly is attributed to the emergence of possible local electric polarizations whose inversion symmetry is broken by inhomogeneously distributed stacking faults. A field-induced intermediate phase is only observed when a magnetic field is applied perpendicular to the Ru-Ru bonds for samples with minimal stacking faults. Less pronounced in-plane anisotropy is found in samples with sizable contribution from stacking imperfections. Our findings suggest that dielectric measurement is a sensitive probe in detecting the structural and magnetic properties, which may be a promising tool especially in studying $\alpha$-RuCl$_3$ thin film devices. Moreover, the stacking details of RuCl$_3$ layers strongly affect the ground state both in the magnetic and electric channels. Such a fragile ground state against stacking faults needs to be overcome for realistic applications utilizing the magnetic and/or electric properties of Kitaev based physics in $\alpha$-RuCl$_3$.

I. INTRODUCTION

The possible emergence of Majorana fermion excitations in a $S = 1/2$ Kitaev quantum spin liquid (QSL) state is thought to be a promising channel to realize topological quantum computing [1, 2]. Solvability of the honeycomb Kitaev model has boosted the experimental interests to search for real materials in which Kitaev physics is at play. Some Mott insulators with strong spin-orbit coupling induced effective spin-1/2 ($J_{\text{eff}} = 1/2$) appear to be promising candidates of Kitaev materials [3–5]. To date, a few possible compounds including iridates ($A_2\text{IrO}_3$, $A$=Li, Na) [6–11] and ruthenates ($\alpha$-RuCl$_3$) [12–22] have been found, although conclusive evidence is still lacking.

Of particular interest is the layered compound $\alpha$-RuCl$_3$, which is in close proximity to the ideal Kitaev model although a zigzag antiferromagnetic (AF) order is favored at low temperatures due to sizable Heisenberg interactions and non-zero off diagonal terms [4, 12, 23, 24]. The AF ground state is unstable against application of pressure [18, 25, 26] and in-plane magnetic fields [19, 27–31]. The system enters a quantum disordered phase when an in-plane magnetic field is higher than a critical value of $\mu_0 H_c \sim 8$ T is applied. Evidence of fractional excitations emerged from this field-induced quantum disordered state has been reported by various techniques [22, 27, 32], but the nature of this phase is still under debate. Meanwhile, the magnetic transition is very sensitive to the stacking sequence of the honeycomb layer. It has been suggested that a stacking of $ABC$ series produces the AF transition at $T_{N1} \sim 7$ K, and that an $ABAB$ stacking is responsible for the transition at $T_{N2} \sim 14$ K [13]. Neutron scattering experiments indeed found non-negligible interlayer magnetic interactions [29, 33], which necessarily couple to the details of layer stacking. Stacking faults can be easily formed due to weak interlayer van-der-Waals bonding (< 1 meV [34]) and the small energy difference between these two configurations. Formation of stacking faults has been evidenced by the appearance of multiple magnetic transitions within one sample [13, 16]. To date, big progress has been made to unravel the interplay between magnetic, lattice and Kitaev interactions both theoretically and experimentally. However, less effort has been applied to the study of stacking faults and their related magnetic properties from the charge and/or electric degrees of freedom, which are also important aspects to understand the ground state and for future real device applications.

In this article, we report on the out-of-plane dielectric and magnetodielectric measurements of $\alpha$-RuCl$_3$ single crystals with different degrees of stacking faults. A frequency dependent dielectric anomaly is observed at $T_A (f = 100\text{kHz}) \sim 4$ K in samples showing both magnetic transitions at $T_{N1} \sim 7$ K and $T_{N2} \sim 14$ K. Suppression of the magnetic transitions using in-plane magnetic fields produces negligible effect on the observed dielectric anomaly. No signature of such a dielectric anomaly is found in crystals with the dominant transition at $T_{N1} \sim 7$ K. We conclude that the observed dielectric anomaly likely originates from local electric polarizations, which appear at the interfaces between $ABC$ and $ABAB$ stacking. The inversion symmetry is possibly broken by inhomogeneous distribution of stacking faults. The mag-

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netodielectric effect is found to be anisotropic for in-plane magnetic fields applied parallel and perpendicular to the Ru-Ru bonds. The field-induced intermediate state found in earlier reports with magnetic fields applied perpendicular to the Ru-Ru bonds [29, 33], is confirmed by our magnetodielectric measurements for samples with minimal stacking faults. Our results suggest that the complex magnetic phases in α-RuCl₃ can also be accessed by dielectric probe, and that the structural details determine the ground state both in the magnetic and electric channels.

II. METHODS

α-RuCl₃ single crystals were grown by chemical vapour transport method in a two-zone furnace. Commercial RuCl₃ powders (3 g in mass, Furuya metal) were first sealed in a quartz tube (length: 12 cm, diameter: 2 cm) and then put in the two-zone furnace (source temperature 790 °C, sink temperature 710 °C). Black shiny plates of α-RuCl₃ single crystals would appear at the sink end after dwelling for 5 days. The samples used in this study have typical dimension of 5×5×0.3 mm³. The dielectric constant of the α-RuCl₃ single crystals was measured by an Agilent E4980A LCR meter with electric field applied perpendicular to the ab plane (E || c in the R3 notation) in a 9 T Quantum Design Dynacool System and a 14 T Oxford Cryostat. The electrodes were prepared by sputtering 50 nm Au on both sides of the ab crystal surfaces. The heat capacity measurements were performed in a 9 T Quantum Design Dynacool System.

III. RESULTS AND DISCUSSIONS

A. Structural and Magnetic Transitions

The normalized dielectric constants, ε(T)/ε₃₀₀K, of three typical α-RuCl₃ single crystals measured at zero magnetic field are presented in Figure 1(a–c). The electric field was applied perpendicular to the ab plane (E || c). The room temperature relative dielectric constant, ε₀(300 K) = ε/ε₀ = Cd/ε₀A, was estimated to be ∼15 for all three samples. Here, ε₀ is the dielectric constant of vacuum, C is the measured capacitance, d is the sample thickness, A is the effective area of the electrodes deposited on sample surfaces. Hysteretic step-like features appearing at Tₑ || c (upon cooling) and Tₑ || c (upon warming) are clearly seen in all samples, which are signatures of a first-order structural transition. Evidence of such a structural transition has also been captured by other techniques, including heat capacity [35], magnetization [16], X-ray [17], Raman scattering [14], thermal-expansion [26, 28, 35, 36] and an earlier dielectric study [37]. Instead of the high-temperature monoclinic C2/m structure, it is likely that a different phase is formed at low temperatures (trigonal P3112 or rhombohedral R3̅ phase [17, 31, 38]). However, the origin of this structural transition remains unclear. Here we adopt the R3̅ convention for convenience. Given the nature of weak van-der-Waals bonding, formation of stacking faults is inevitable during such a hysteretic transition. Only one dominant magnetic transition occurring at either TN₁ ∼ 7 K or TN₂ ∼ 14 K would be expected if a crystal has minimal stacking faults. As shown in Fig. 1(d), this case is realized in Sample 1 which shows a dominant sharp peak at TN₁ = 7.3 K in the specific heat data. For Sample 2 and Sample 3, another step-like feature appears at TN₂ = 14 K in addition to the major peak locating at TN₁ [see Figs. 1(e) and 1(f)]. This simply indicates a considerable mixing of ABC and ABAB polymorphs and sizable stacking faults [13]. Different degrees of stacking faults in the three samples studied here are likely caused by careless handling during electrodes preparation [13]. Note that a broad hump sitting around 10 K is also visible in Sample 3. Similar feature has been reported earlier [16, 21, 26], whose origin is attributed to competing exchange interactions [16]. Although the exact nature is yet to be clarified, sizable stacking faults certainly play an important role.

The width of the hysteretic structural transition Tₑ || c = Tₑ − Tₑ, also correlates with the degree of stacking faults. Compared to Sample 1, more and more stacking faults are introduced into Sample 2 and Sample 3 as evidenced by the heat capacity results. Correspondingly, Tₑ || c spans over a larger and larger temperature range for Sample 2 and Sample 3. It is likely that when cooled below Tₑ, the transformation between the high-temperature and low-temperature phases is less complete for Sample 2 and Sample 3 than for Sample 1 [26, 36]. Naturally, more stacking faults are formed and a larger hysteresis is necessary to restore the high temperature structure upon warming. Note that the dielectric constant is generally not fully recovered after Tₑ upon warming, although the lattice constants are more or less restored [26, 28, 35, 36]. This implies that the formed stacking faults are irreversible when passing through the structural transition, and that the dielectric probing is sensitive to these minute structural perturbations. Reversible dielectric constant is eventually achieved near room temperature when thermal energy is strong enough to wipe out these tiny structural differences.

B. Dielectric Anomaly

In Fig. 2, we present the temperature dependence of the normalized dielectric constant, ε/ε₂₀K, near the AF transitions region. The magnetic fields were applied along the Ru-Ru bonds [H || (1,0,0) in the reciprocal space, see inset of Fig. 2(a)]. No significant differences are found when applying magnetic fields perpendicular to the Ru-Ru bonds for temperature sweep (data not shown here). Clearly, these three samples have different dielectric response with respect to temperatures and external
by thermal-expansion measurements \cite{26, 28}. Upon application of in-plane magnetic fields, $C_p/T$ of Sample 1 decreases continuously with cooling in all fields (Fig. 2(a)). At zero field, only a step-like jump appears at $T_{N1} = 7.5$ K [determined by the peak in $dC_p/dT$, see the inset of Fig. 2(d)], below which the dielectric constant is slightly reduced. This magnetic order induced dielectric reduction is a possible signature of a type-II multiferroic as discussed by J. Zheng et al. \cite{37}. Another more trivial explanation could be simple enhancement of the $c$-axis lattice constant caused by magnetoelastic coupling as found by thermal-expansion measurements \cite{26, 28}. Upon application of in-plane magnetic fields, the AF transition at $T_{N1}$ shifts gradually towards lower temperatures and eventually vanishes above the critical field $\mu_0 H_{c1} \sim 8$ T. Suppression of $T_{N1}$ by in-plane magnetic fields has also been detected by other techniques, which is thought to be an prominent way for driving the system into the QSL state \cite{19, 27-31}.

In contrast to Sample 1, a negative linear slope is found in Sample 2 [see the inset of Fig. 2(b)] when cooled down from 20 K. This linear temperature dependence deviates below $T_{N2} \sim 14$ K, indicating the appearance of the AF order in the $ABAB$ polymorph. Further cooling leads to a step-like jump at $T_{N1} = 7.5$ K in small fields. Note that the size of the dielectric reduction occurring at $T_{N1}$ is similar in all three samples, as shown in Fig. 2(d), but the transition appears to be sharpest in Sample 1 as expected [see the inset of Fig. 2(d)]. In addition to the magnetic transitions, a dielectric anomaly emerges at a lower temperature $T_A \sim 4$ K for $f = 100$ kHz, which is absent in Sample 1. As illustrated in Fig. 2(e), this dielectric anomaly is accompanied by sizable dissipation, and $T_A$ is defined as the temperature where the dissipation shows a peak. The dielectric anomaly becomes less visible in the intermediate field region (about 5 T to 7 T) as $T_{N1}$ is pushed gradually towards $T_A$. However, a clear signature is recovered again at $\mu_0 H = 9$ T once the AF order formed below $T_{N1}$ is fully suppressed. The dissipation peak [Fig. 2(e)], however, stays nearly intact throughout the studied field range. This implies little effect on the dielectric anomaly by applying in-plane magnetic fields.

The dielectric anomaly becomes the dominant feature in Sample 3 [Fig. 2(c)], and a significant amount of dielectric constant is lost at $T_A$. A clear peak is seen in the dissipation at $T_A$, as shown in Fig. 2(f), which is field independent up to 14 T. As indicated by the specific heat data (see Fig. 1), Sample 2 and Sample 3 have a higher degree of stacking faults. Thus, the observed dielectric anomaly correlates strongly with the degree of stacking faults. An earlier study performed by T. Aoyama et al. \cite{39} reported such a dielectric anomaly for both $E \parallel c$ and
Figure 2. (a-c) Temperature evolution of $\varepsilon/\varepsilon_{20K}$, recorded at $f = 100$ kHz. In-plane magnetic fields were applied along the reciprocal space $(1,0,0)$ direction [parallel to the real space Ru–Ru bonds, see inset in (a)]. Curves have been shifted vertically for clarity. (d) The enlarged view of $\varepsilon/\varepsilon_{10K}$ near $T_{N1}$. The empty squares are experimental raw data and the lines are guides to the eyes. The inset of (d) shows $d\varepsilon/dT$. (e) and (f) The dissipation $(D)$ as a function of temperature measured in fixed fields of Sample 2 and Sample 3, respectively. Inset in (a): an illustration of the in-plane reciprocal space (inner purple hexagon) and real space (outer blue hexagon) representations. Solid triangles in (a-c) track the variation of $T_{N1}$ with respect to in-plane magnetic fields. Vertical dash lines in (b) and (c) mark the dielectric anomaly and the transition at $T_{N2}$ [determined by specific heat data in Fig. 1(e,f)].

Figure 3. Frequency dependency of (a)(c)(e): $\varepsilon/\varepsilon_{20K}$ and (b)(d)(f): the corresponding dissipation $(D)$ of all samples measured in zero field. The dielectric anomaly depends strongly on frequency and $T_A$ shifts gradually to higher temperatures for increasing frequency. (g) A schematic illustration of inversion symmetry breaking caused by non-uniformly distributed stacking faults. Black (red) cross marked out by dash rectangle labels the inversion center of each ABC (AB) unit. The inversion counterpart is missing for the bottom ABC segment when an AB unit is inserted asymmetrically. Inset in (e) and (f) is a fitting of the frequency dependency of $T_A$ according to the Vogel-Fulcher law $f = f_0 \exp \left[ -E/k_B (T_A - T_0) \right]$ using the Boltzmann constant $k_B$, a temperature constant $T_0 = -4$ K, an activation energy $E = 143$ K and a characteristic frequency $f_0 = 7.6 \times 10^{12}$ Hz.
$E \parallel ab$ in samples with major transition at $T_{N2} \sim 14$ K. On the other hand, J. Zheng et al. [37] only found a step-like dielectric reduction at $T_{N1} \sim 7$ K for $E \parallel c$ in samples with minimal stacking faults. T. Aoyama et al. [39] suggested that zigzag AF order induced local polarizations are responsible for the observed dielectric anomaly in the case of $E \parallel ab$. However, unlike the AF transitions which fade away above $\mu_0H_{c2} \sim 10$ T [see [16, 39] and Fig. 4(e,f)], the observed dielectric anomaly for $E \parallel c$ appears to be robust up to 14 T, as shown in Figs. 2(c) and 2(f). Moreover, the dielectric loss for $E \parallel c$ below $T_A$ is much more profound in Sample 3 (about $5 \times 10^{-3}$) than that of crystals with less stacking faults (negligible dielectric loss in Sample 1 and Sample 2. $\sim 5 \times 10^{-4}$ dielectric loss in samples with dominant $ABAB$ stacking [39]). Therefore, it is likely that the dielectric anomaly found here for $E \parallel c$ is more closely associated with stacking faults than the zigzag AF order.

To further unravel the nature of the observed dielectric anomaly, its frequency dependency is explored in Figure 3. Clearly, the dielectric anomaly is strongly frequency dependent. As shown in Fig. 3(c)-(f), $T_A$ moves monotonically towards higher temperatures for increasing frequency. Therefore, any long-range order can be ruled out, as no frequency dependency would be expected. Similar frequency dependency of the dielectric anomaly is also found for $E \parallel ab$, and its origin is attributed to a glassy state of zigzag AF order induced local electric polarizations [39]. As displayed in the inset of Figs. 3(c) and 3(f), the frequency dependency of $T_A$ can be well described by the Vogel-Fulcher law $f = f_0 \exp\left[-E/k_B(T_A - T_0)\right]$ with similar $T_0 = -4$ K, activation energy $E = 143$ K and characteristic frequency $f_0 = 7.6 \times 10^{12}$ Hz compared to those of $E \parallel ab$ [39]. This suggests that the same physics is at play for both $E \parallel ab$ and $E \parallel c$, i.e., a possible glassy state of local electric polarizations is formed. Such an argument is plausible as the characteristics of dipolar glasses [40], spin glasses [41] and relaxor ferroelectrics [42] can be described by similar phenomenological Vogel-Fulcher approach. Given the negligible response to in-plane magnetic fields, the electric polarizations here for $E \parallel c$ are most probably caused by stacking faults located at the $ABC/ABAB$ interfaces. As sketched in Fig. 3(g), the inversion center sits in the middle of $B$ layer in each $ABC$ unit of pure $ABC$ stacking. The bottom $ABC$ segment could not find its inversion counterpart if an $AB$ unit was inserted asymmetrically into $ABC$ layers. We note that a uniform distribution of stacking faults still preserves the inversion symmetry. Instead of zigzag AF order induced symmetry breaking in the $ab$ plane, here along the $c$-axis, the inversion symmetry is broken locally by inhomogeneously distributed stacking faults.

### C. Magnetodielectric Effect and Field induced Intermediate State

In this section, we study the anisotropic magnetodielectric effect and the results are presented in Figure 4. In-plane anisotropy and multiple field induced magnetic phase transitions are clearly seen in all samples. In the paramagnetic state above $T_{N1}$ or $T_{N2}$, the magnetodielectric data generally show temperature independent backgrounds, which vary between samples and field directions. This discrepancy might be caused by sample and thermal history dependent stacking faults as measurements for different field orientations were performed after several thermal cycles up to room temperature.

For Sample 1 shown in Figs. 4(a) and 4(b), a local minimum at $\mu_0H_c \sim 4$ T is observed consistently below $T_{N1}$ along both field directions. This dip feature is likely associated with the domain repopulation as found by neutron scattering experiments [43]. The domain reorientation apparently exists in all samples. The transition from the AF ordered state to the quantum disordered phase is evidenced by a step-like jump sitting at $\mu_0H_{c1} \sim 8$ T in Sample 1 and Sample 2. Additionally, a small bump is found at $\mu_0H_{c2} \sim 6$ T for $E \parallel (1,2,0)$ only (perpendicular to the Ru-Ru bonds), which is more pronounced in Sample 2 [see Fig. 4(d)]. This field-induced intermediate phase between $H_x$ and $H_1$, with field applied perpendicular to the Ru-Ru bonds has also been evidenced by AC susceptibility and inelastic neutron scattering experiments [29, 33], although its origin still remains elusive.

Figures 4(c) and 4(f) display the results of Sample 3. An additional peak appears at $\mu_0H_{c2} \sim 10$ T below $T_{N2}$, apart from familiar features at $\mu_0H_r$ and $\mu_0H_{c1}$. Apparently, a higher field is necessary to partially align the zigzag order formed below $T_{N1}$ [16, 39]. Compared to other two samples, the critical field $\mu_0H_{c1}$ for suppressing the AF zigzag order formed below $T_{N1}$ is reduced from $\sim 8$ T to $\sim 6$ T at 2 K. The field induced intermediate phase is not visible in Sample 3 due to the close proximity between $\mu_0H_{c1}$ and $\mu_0H_x$.

### D. Phase Diagram

In Figure 5, we summarize the $T$–$H$ phase diagrams of the three different samples studied here. The data points were extracted from the dielectric, magnetodielectric and specific heat results. One sees that all the phases found by other techniques have been mapped out nicely using dielectric probing. Similarities can be found in Sample 1 and Sample 2 where the magnetic phase is mainly governed by the AF zigzag order formed below $T_{N1}$. Clear in-plane anisotropies are found for these two samples. For $H \parallel (1,0,0)$, main features take place at the domain repopulation field $\mu_0H_r$ and the suppression of AF order crossing the $\mu_0H_{c1}$ lines. An additional field induced intermediate $X$ state shows up between $\mu_0H_x$ and $\mu_0H_{c1}$ for $H \parallel (1,2,0)$ in Sample 1 and Sample 2. Less
Figure 4. Magnetodielectric effect measured at fixed temperatures and constant frequency $f = 100$ kHz. In (a) and (b), magnetic fields were along and perpendicular to the Ru-Ru bonds with $\mathbf{H} \parallel (1,0,0)$ and $\mathbf{H} \parallel (1,\bar{2},0)$, respectively for Sample 1. (c)(d) and (e)(f): same measurements with (a)(b) for Sample 2 and Sample 3, respectively. Curves are shifted vertically for clarity.

Figure 5. $T-H$ phase diagrams of the studied three samples derived from Fig. 2 and Fig. 4. (a) and (b): $T-H$ phase diagrams of Sample 1 with fields applied along the $\mathbf{H} \parallel (1,0,0)$ and $\mathbf{H} \parallel (1,\bar{2},0)$, respectively. (c)(d) and (e)(f): Same representations to those of (a)(b) for Sample 2 and Sample 3, respectively. The symbols ZZ3 and ZZ2 represent three and two domains in the zigzag phase, respectively. The field induced intermediate state is labeled as the X phase. The paramagnetic state is labeled as PM and the zigzag AF order formed below $T_{N2}$ is represented as AFM 2. Green dots were obtained in specific heat experiments.

anisotropy appears in Sample 3 which has a sizable degree of stacking faults. Both transitions at $\mu_0 H_r$, $\mu_0 H_{c1}$ and $\mu_0 H_{c2}$ are identified, whereas the intermediate state is missing due to the collapsing of $\mu_0 H_{c1}$ onto $\mu_0 H_x$. The stacking faults induced glassy phase of electric dipoles observed in Sample 2 and Sample 3 is not shown in the phase diagram, as it is not a long-range order. By comparing these three samples, it is clear that the ground state of $\alpha$-RuCl$_3$ is very sensitive to structural details both in the magnetic and electric channels due to strong interplay between lattice, spin and charge degrees of freedom.

IV. CONCLUSIONS

In summary, we observe an out-of-plane dielectric anomaly in $\alpha$-RuCl$_3$ which appears to be closely associated with inhomogeneously distributed stacking faults. This dielectric anomaly is a signature of a possible glassy
state of local electric polarizations, which is evidenced by its strong frequency dependency and sizable dissipations. Immunity to strong external in-plane magnetic fields of this glassy state points to a structural origin instead of a magnetic root. Details of the magnetic phase diagram, including the domain repopulation, the field-induced intermediate (field applied perpendicular to the Ru-Ru bonds) and the transition between AF ordered and disordered phases, were successfully mapped out using dielectric and magnetodielectric probing. The dielectric probing may thus serve as a promising tool for detecting stacking faults and studying the magnetic properties of $\text{α-RuCl}_3$ thin film devices when bulk measurements are not accessible. Our findings also suggest that the ground state is rather fragile against structural perturbations both in the magnetic and electric channels. Further efforts are needed to overcome this difficulty and to eventually manipulate the novel Kitaev physics in $\text{α-RuCl}_3$ based devices.

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