A Theoretical Investigation on CO Oxidation by Single-Atom Catalysts M$_1$/$\gamma$-Al$_2$O$_3$ (M = Pd, Fe, Co, and Ni)

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Single-atom catalysts have attracted much interest recently because of their excellent stability, high catalytic activity, and remarkable atom efficiency. Inspired by the recent experimental discovery of a highly efficient single-atom catalyst Pd$_x$/$\gamma$-Al$_2$O$_y$, we conducted a comprehensive DFT study on geometries, stabilities, and CO oxidation catalytic activities of M$_1$/$\gamma$-Al$_2$O$_3$ (M = Pd, Fe, Co, and Ni) by using slab-model. One of the most important results here is that Ni$_x$/Al$_2$O$_3$ catalyst exhibits higher activity in CO oxidation than Pd$_x$/Al$_2$O$_3$. The CO oxidation occurs through the Mars van Krevelen mechanism, the rate-determining step of which is the generation of CO$_2$ from CO through abstraction of surface oxygen. The projected density of states (PDOS) of 2p orbitals of the surface O, the structure of CO-adsorbed surface, charge polarization of CO and charge transfer from CO to surface are important factors for these catalysts. Although the binding energies of Fe and Co with Al$_2$O$_3$ are very large, those of Pd and Ni are small, indicating that the neighboring O atom is not strongly bound to Pd and Ni, which leads to an enhancement of the reactivity of the O atom toward CO. The metal oxidation state is suggested to be one of the crucial factors for the observed catalytic activity.

Introduction

Nanoparticles supported on metal oxides have been recognized to have high catalytic activity towards numerous reactions such as CO oxidation, NO reduction, and water-gas shift reaction.[1–5] Nanoparticle-catalyzed CO oxidation, which can remove CO from car exhausts and purify H$_2$ in polymer electrolyte membrane fuel cells, is usually used as a benchmark to evaluate the performance of various supported metal catalysts.[6]

Compared with isolated metal nanoparticles, the presence of metal-oxide surfaces as well as strong metal-support interactions changes the electronic structures of metal clusters,[7] lowers activation barriers, and provides new reaction pathways. The metal-oxide supports are generally divided into reducible and irreducible metal oxides.[2] The reducible metal oxides (TiO$_2$, CeO$_2$, FeO$_x$, etc.) can provide labile oxygen species that participate in the reaction. On the other hand, Al$_2$O$_3$ and MgO usually belong to the class of the irreducible metal oxides. Some experimental works revealed that the catalytic activity of supported metal nanoparticle depends remarkably on its size and shape,[8, 9] because the number of low-coordinated atoms in metal nanoparticles, which often function as active sites in catalytic reaction, increases dramatically as the size of nanoparticles decreases. Therefore, single-atom catalysts supported on metal oxides, in which an isolated metal atom is anchored to a support, attract wide interest, not only because of their low-temperature activity but also because of their atom efficiency, stability, and selectivity.[10–16]

In 2011, Qiao et al. successfully synthesized a single-atom catalyst with Pt atoms uniformly dispersed on a reducible FeO$_x$ support, Pt$_x$/FeO$_x$, which shows excellent stability and high activity for CO oxidation. It is noted that this catalyst performs preferential oxidation of CO in CO–H$_2$ mixture.[17] Then, the same group reported a theoretical and experimental study on Ir$_x$/FeO$_x$.[18] Recently, using density functional theory (DFT) calculations, Li et al. investigated a series of single-atom catalysts, M$_x$/FeO$_x$ (M = Au, Rh, Pd, Co, Cu, Ru, and Tl).[19] They found that under the Langmuir-Hinshelwood (LH) mechanism, the catalyt-
ic performance of single Rh, Pd, Ru, and Ti atoms on iron oxide surface is even higher than that of Pt/FeOx for CO oxidation. Moreover, Qiao and co-workers also synthesized a single-atom catalyst AuM/CoOx and examined its catalytic activity toward CO oxidation.\(^{28}\) Very recently, a series of single-atom catalysts with Au were investigated with both experimental and theoretical studies.\(^{21–23, 25}\) Liang et al. proposed theoretically an efficient single-atom catalyst Ni\(_2\)/FeO\(_x\).\(^{24}\)

On the other hand, several groups focused on single-atom catalysts supported on irreducible metal oxides. In 2001, Abbet et al. studied CO oxidation on single Pd atom supported on oxygen-defective MgO(100).\(^{25}\) Their experimental and theoretical investigations revealed that as the CO oxidation reaction proceeds, oxygen vacancies will anneal, resulting in coalescence of the remaining Pd to form large clusters. By means of ab initio molecular dynamics, Ghosh and Nair investigated the LH mechanism of CO oxidation on Rh\(_x\)/\(\gamma\)-Al\(_2\)O\(_3\).\(^{26}\) Narula and co-workers performed experimental and DFT research on CO oxidation on a single-atom catalyst Pt\(_x\)/\(\alpha\)-Al\(_2\)O\(_3\)(010) and proposed a modified LH mechanism to explain the catalytic activity.\(^{27}\) Although Al\(_2\)O\(_3\) is chemically inert and thermodynamically stable, the supported noble metal catalysts, such as Rh, Pt and Au, can also promote the participation of the oxygen atoms of Al\(_2\)O\(_3\) in chemical reactions.\(^{26, 28–29}\) Very recently, Peterson et al. reported that single Pd atom anchored in \(\gamma\)-alumina has both high stability and catalytic activity toward CO oxidation.\(^{30}\) They proposed that even though \(\gamma\)-alumina belongs to the irreducible metal oxides, the reaction follows the Mars van Kreeven (MvK) mechanism, in which the surface oxygen participates in the reaction, because of the fact that Pd is anchored rather than supported on the surface. Because Rh, Pd, and Pt are all precious metals, it is highly meaningful to find more efficient and low-cost single-atom alternative catalysts supported on irreducible metal oxides.

In the present work, we investigated CO oxidation by various single-atom catalysts anchored on \(\gamma\)-alumina (M\(_x\)/\(\gamma\)-Al\(_2\)O\(_3\)), consisting of abundant 3d metals such as Fe, Co, and Ni and compared their catalytic performance with Pd\(_x\)/\(\gamma\)-Al\(_2\)O\(_3\) using a DFT method with slab-model. Our main purposes here are to predict whether a 3d metal single-atom catalyst is useful for the CO oxidation reaction, to elucidate the reaction mechanism, to clarify the rate-determining step, and to disclose important factor(s) for catalytic activity.

**Results and Discussion**

**Geometries and Stabilities of M\(_x\)/\(\gamma\)-Al\(_2\)O\(_3\) (M = Pd, Fe, Co, and Ni)**

Previous DFT calculations revealed that the adsorption energy of Pd on \(\gamma\)-alumina is in the order of 1.0–1.3 eV and the diffusion barrier of supported Pd atoms on \(\gamma\)-alumina(1 0 0) is about 0.3 eV, suggesting that supported Pd atoms can diffuse easily on surfaces and nucleate quickly to form large clusters.\(^{31, 32}\) Furthermore, X-ray absorption near edge structure (XANES) analysis suggested that Pd on the alumina surface has a four-fold coordination with oxygen atoms.\(^{33}\) It is reasonable to predict that the Pd atom replaces an Al atom and is embedded in the alumina surface. This model is consistent with the above mentioned experimental observation and the large binding energy of Pd with Al\(_2\)O\(_3\) prevents Pd atoms from diffusing on the surface.

To simulate the \(\gamma\)-alumina surface, a periodic slab model of the dehydrated \(\gamma\)-Al\(_2\)O\(_3\)(1 0 0) surface was chosen, which is the same as that used by Peterson and co-workers.\(^{30}\) As shown in Figure 1, there are four non-equivalent Al atoms on the surface. To find a suitable site for Pd and other metals, we calculated the formation energy (\(\Delta E(Al_{vac})\)) of an Al vacancy (Al\(_{vac}\)). The \(\Delta E(Al_{vac})\) is obtained through Equation (1):

\[
\Delta E(Al_{vac}) = E_{Alvac} + E_{Al} - E_{pistina}
\]

where \(E_{Alvac}\), \(E_{Al}\) and \(E_{pistina}\) are the total energies of the slab with an Al vacancy, the isolated Al atom and the pristine slab, respectively. The smaller \(\Delta E(Al_{vac})\) is, the easier formation of an Al vacancy is. The calculated \(\Delta E(Al_{vac})\) values of four different Al vacancies are 13.10, 13.85, 13.94, and 13.93 eV, respectively. The \(\Delta E(Al_{vac})\) of site A (Figure 1) has the smallest value, which is the same as the results of Peterson et al.\(^{30}\) As samples were calcined at high temperature for one hour in ambient air in the process of catalyst preparation, the thermal stability is also very important.\(^{30}\) We calculated the relative energies of Pd\(_x\)/Al\(_2\)O\(_3\) with Pd anchoring in four different sites and found that Pd\(_x\)/Al\(_2\)O\(_3\) with Pd in site A has the lowest relative energy. Consequently, a doping metal atom such as Pd prefers to be embedded in site A.

Next, we focused on binding energies and geometric and electronic properties of M\(_x\)/Al\(_2\)O\(_3\) (M = Pd, Fe, Co, and Ni), which are shown in Table 1. The binding energy \(E_b\) is obtained

![Figure 1](image-url)
through Equation 2:
\[ E_b = E_{\text{Alvac}} + E_{\text{metal}} - E_{\text{tot}} \]  
where \( E_{\text{Alvac}} \), \( E_{\text{metal}} \) and \( E_{\text{tot}} \) are total energies of the slab with an Al vacancy, the isolated metal atom and the slab doped with \( M \), respectively. Compared with the binding energy \( E_b \) of Pd, the \( E_b \) of Fe, Co and Ni are theoretically evaluated to be much larger, indicating that these nanocomposites are easily formed on generation of an Al vacancy. Using a Bader charge analysis, it is found that considerable charge transfer from metal atom to Al\(_2\)O\(_3\) occurs. Comparison of \( M \) with Al provides clearer features. Al exhibits the largest \( E_b \) and the largest positive charge. Consequently, the surrounding O atoms interact well with Al and receive enough population. As a result, the surface O atoms are stable and not reactive. For Pd and Ni, \( E_b \) is small and M positive charge is small, suggesting that the surrounding O atoms do not interact well with Pd and Ni, and therefore, they are active, which will be discussed below. There is a good correlation between binding energy and charge value, suggesting that the greater the atomic charge is, the larger the binding energy becomes; in other words, charge-transfer and electrostatic interactions could be relevant for M-support interaction.

Mechanism of CO Oxidation on \( M_1/\gamma\)-Al\(_2\)O\(_3\) (\( M = \) Pd, Fe, Co, and Ni)

The experimental study revealed that for the CO oxidation on Pd\(_1/\gamma\)-Al\(_2\)O\(_3\), the orders of reaction rates are +0.35 and +0.15 with respect to CO and O\(_2\), respectively.\(^{[30]}\) Thus, it was experimentally proposed that the reaction mechanism follows the MvK mechanism, in which the oxygen atoms are originate from the surface rather than from the gas. Theoretical calculations by Peterson and co-workers also confirmed the low energy barrier of the MvK mechanism for this system.\(^{[30]}\)

As shown in Scheme 1, the reaction begins by CO adsorption to the metal in an end-on structure to afford a CO-adduct 2. Via a transition state 3TS, the adsorbed CO reacts with the nearby lattice oxygen and forms OCO\(^*\) on the surface. The OCO\(^*\) leaves the surface through a transition state 5TS to form an intermediate 6 in which CO\(_2\) is adsorbed on the surface. The adsorbed CO\(_2\) is easily released to afford an intermediate 7 with an oxygen vacancy on the alumina surface. Then, an O\(_2\) molecule adsorbs on the surface to afford an intermediate 8, in which one O atom interacts with the metal atom and the other O is in the oxygen vacancy. The following step is the adsorption of the second CO to the metal, forming an intermediate 9. Via a transition state 10TS, the second CO reacts with the pre-adsorbed O on the metal-oxide surface to form the second CO\(_2\).

The above reaction cycle can be described by four steps, as shown in chemical Equations (3)–(6):

\[ \text{OCO}^* + \text{O}_{\text{lattice}} \rightarrow \text{OCO}_{\text{lattice}}^* \]  
\[ \text{OCO}_{\text{lattice}}^* \rightarrow \text{CO}_2 + \text{O}_{\text{vac}} \]  
\[ \text{CO} + \text{O}_2 + \text{O}_{\text{vac}} \rightarrow \text{OC}^* + \text{O}^*_{\text{lattice}} \]  
\[ \text{OC}^* + \text{O}^*_{\text{lattice}} \rightarrow \text{CO}_2 + \text{O}_{\text{lattice}} \]

Except for step (3) (Equation (5)), the other three steps have energy barrier. The key steps shown in Equations (3) and (6) satisfy the MvK mechanism. The geometries of those structures are shown in Figure 2, and relative energies and energy barriers are presented in Table 2 and Figure 3. Parameters such as bond distances are presented in the Supporting Information.

Whether or not the CO oxidation catalyst can efficiently capture adsorbates such as CO and O\(_2\) is very important for their further catalytic cycle.\(^{[19]}\) In general, it is recognized that intermediates able to participate in a catalytic reaction should not be too stable or too unstable. As shown in Table 2 and Figure 3, the CO adsorption energy of the first CO molecule is quite different for each \( M \), while the second CO adsorption energy is quite different for each \( M \) (Pd, Fe, Co, and Ni) catalyst. Fe/Al\(_2\)O\(_3\) and Co/Al\(_2\)O\(_3\) exhibit the smallest and largest CO adsorption energies, 0.28 and 1.41 eV, respectively.
the CO adsorption energies for Pd$_1$/Al$_2$O$_3$ and Ni$_1$/Al$_2$O$_3$ are similarly moderate as 0.74 and 0.77 eV, respectively.

In step (1) (Equation (3)), which corresponds to the OCO$_{\text{lattice}}$* formation, the energy barrier of the Pd$_1$/Al$_2$O$_3$-catalyzed reaction is calculated to be 0.30 eV, similar to the report by Petersson et al. (0.26 eV) at the PW91 level. The moderate difference may be ascribed to the use of a different density functional. Fe$_1$/Al$_2$O$_3$ and Co$_1$/Al$_2$O$_3$-catalyzed reactions need energy barriers (0.32 and 0.42 eV) comparable to that of Pd$_1$/Al$_2$O$_3$. However, the energy barrier of the Ni$_1$/Al$_2$O$_3$-catalyzed reaction is as low as 0.16 eV. This process is exothermic with reaction energies ranging from 0.08 to 0.42 eV except for the Co$_1$/Al$_2$O$_3$ catalyzed one.

The energy barrier of OCO$_{\text{lattice}}$* desorption from the surface depends strongly on the nature of the metal atom in step (2) (Equation (4)). For Pd$_1$/Al$_2$O$_3$, the energy barrier is 0.90 eV. Interestingly, the calculated energy barrier of Ni$_1$/Al$_2$O$_3$ is 0.52 eV, much lower than that of Pd$_1$/Al$_2$O$_3$. In contrast, Fe$_1$/Al$_2$O$_3$ and Co$_1$/Al$_2$O$_3$-catalysts need very high energy barriers of 1.49 and 1.20 eV, respectively. Notably, this process is endothermic for all four single-atom catalysts. The release of physically adsorbed CO$_2$ from the surface is slightly endothermic.

In step (4) (Equation (6)), in which the second CO$_2$ formation occurs, the barrier of the Pd$_1$/Al$_2$O$_3$-catalyzed reaction is calculated to be 0.22 eV, similar to the previous result of 0.27 eV. In step (1) (Equation (3)), PBE gives a moderately higher energy barrier than PW91 whereas the PBE result here is moderately lower than PW91 one. All of the other three catalysts need low energy barriers ranging from 0.07 to 0.41 eV.

Overall, the reaction of CO with surface oxygen to generate the first CO$_2$ molecule is the rate-determining step of the whole catalytic cycle. For Ni$_1$/Al$_2$O$_3$, each energy barrier is evidently lower than the corresponding energy barrier of Pd$_1$/Al$_2$O$_3$. Consequently, from both thermodynamic and kinetic points of view, Ni$_1$/Al$_2$O$_3$ is suggested to exhibit better catalytic performance than Pd$_1$/Al$_2$O$_3$. On the other hand, because of the high energy barrier of step (2) (Equation (4)), the catalytic performance of both Fe$_1$/Al$_2$O$_3$ and Co$_1$/Al$_2$O$_3$ should be worse than that of Pd$_1$/Al$_2$O$_3$. 

![Figure 2. Reaction pathway of CO oxidation on M$_1$/Al$_2$O$_3$ (M = Pd, Fe, Co, and Ni).](image)

![Figure 3. Adsorption energies (BE(1), BE(2), and BE(3)) and energy barriers (Ea(1), Ea(2), and Ea(3)) of three transition states of CO oxidation on M$_1$/Al$_2$O$_3$ (M = Pd, Fe, Co, and Ni).](image)
Origin of the Catalytic Performance of $\text{M}_1/\gamma\text{-Al}_2\text{O}_3$ ($\text{M} = \text{Pd, Fe, Co, and Ni}$)

To clarify the causes leading to such different catalytic performances of the four single-atom catalysts, we analyze their geometric and electronic structures in this section.

As mentioned above, the CO adsorption energy is relevant for the initial step of catalysis. The Bader charge of the metal atom in $\text{M}_1/\gamma\text{-Al}_2\text{O}_3$ in Table 1 could not explain the order of CO adsorption energy on $\text{M}_1/\gamma\text{-Al}_2\text{O}_3$ ($\text{M} = \text{Pd, Fe, Co, and Ni}$). As the CO molecule approaches the metal atom, there are two main orbital interactions between the CO molecule and the metal atom. First, the lone pair orbital of CO interacts with the unoccupied $s$ and $d$ orbitals of the metal atom, resulting in charge transfer from CO to the metal atom. Second, the back-donation takes place from the metal atom to CO through the interaction between the metal atomic $d$ orbital and the CO molecular $\pi^*$ orbital.

We calculated the projected density of states (PDOS) of $s$ and $d$ atomic orbitals of the metal atom in reactant 1, as shown in Figure 4. From the PDOS of M-$s$ orbital, there is an unoccupied $s$ orbital near the Fermi level for Ni$_2$/Al$_2$O$_3$ and Pd$_2$/Al$_2$O$_3$, which interacts with the lone pair orbital of CO. Also, the occupied $d$ orbital is found at higher energy than in Fe$_2$/Al$_2$O$_3$. On the other hand, there are no obvious unoccupied $s$ orbital and occupied $d$ orbitals close to the Fermi level in Fe$_2$/Al$_2$O$_3$. These results indicate that the CO adsorption is stronger in Ni$_2$/Al$_2$O$_3$ and Pd$_2$/Al$_2$O$_3$ than in Fe$_2$/Al$_2$O$_3$. In Co$_2$/Al$_2$O$_3$, there evidently are occupied $d$ orbitals near the Fermi level which are much higher in energy than in Pd$_2$/Al$_2$O$_3$ and Ni$_2$/Al$_2$O$_3$. Therefore, the back-donation with the $\pi^*$ orbital of CO is stronger in Co$_2$/Al$_2$O$_3$ than in Pd$_2$/Al$_2$O$_3$ and Ni$_2$/Al$_2$O$_3$. This is consistent with the result that Bader charge of CO on Co$_2$/Al$_2$O$_3$ is negative whereas those values for Ni$_2$/Al$_2$O$_3$ ($\text{M} = \text{Pd, Fe, and Ni}$) are positive (Table S3 in Supporting Information).

The largest CO adsorption energy with Co$_2$/Al$_2$O$_3$ mainly arises from the strong back-donation. The metal–carbon distance in intermediate 2 of Fe$_2$/Al$_2$O$_3$ is much larger than that of the other three catalysts, in agreement with the weak interaction between CO and Fe$_2$/Al$_2$O$_3$ (Table S3).

To analyze the oxidation state of the doped metal, d-DOS together with the partial charges were used because the $d$ orbital occupation is strongly related to the oxidation state of the metal. Bader charge in Table 1 qualitatively indicates that Ni and Pd have similar oxidation states that are lower than those of Fe and Co. As shown in Figure 4, the PDOS of the $d$ orbitals found in unoccupied levels are much larger in the case of Fe$_2$/Al$_2$O$_3$ and Co$_2$/Al$_2$O$_3$ than for Pd$_2$/Al$_2$O$_3$ and Ni$_2$/Al$_2$O$_3$, suggesting that Fe and Co have higher oxidation states than Ni and Pd. Although it is not easy to define the oxidation state (= II or + III), it is possible to discuss the values qualitatively to support our explanation.

Next, we focus on the first energy barrier $E_1(A)$ of the catalytic cycle. The PDOS of intermediate 2 revealed that for M$_1$/Al$_2$O$_3$ ($\text{M} = \text{Pd, Fe, and Ni}$), the active 2p orbital of O atom (O-p orbital) appears to be located close to the Fermi level, as shown in Figure 5, whereas only tiny conduction band exists in the case of M = Co. For M$_1$/Al$_2$O$_3$ ($\text{M} = \text{Pd and Ni}$), there are occupied and unoccupied O-p orbitals near the Fermi level which interact with $\pi^*$ and lone pair orbitals of CO, respectively, lowering the energy barrier for M$_1$/Al$_2$O$_3$ ($\text{M} = \text{Pd and Ni}$). However, occupied O-p orbital of Fe$_2$/Al$_2$O$_3$ and Co$_2$/Al$_2$O$_3$ only appear at lower energy (~1.0 eV and ~1.5 eV). The Bader charge analysis showed that the positive charge of the carbon atom in CO and

![Figure 4](image-url)

*Figure 4. Calculated projected density of states (PDOS) for M-$s$ orbital (black) and M-$d$ orbitals (red) of M$_1$/Al$_2$O$_3$ ($\text{M} = \text{Pd, Fe, Co and Ni}$).*

![Figure 5](image-url)

*Figure 5. Calculated the projected density of state (PDOS) for O-p orbital of the surface reactive oxygen atom in intermediate 2 of M$_1$/Al$_2$O$_3$ ($\text{M} = \text{Pd, Fe, Co and Ni}$).*
the negative charge of active O in the lattice in Ni₃/Al₂O₃ is large, $1.110 \, |e|$ and $-1.459 \, |e|$, respectively. The spin density in M₄/Al₂O₃ (M=Pd and Ni) is distributed on the doped metal and surface O (Figure S5 in the Supporting Information), indicating that the surface O is evidently activated. From a geometric point of view, as presented in Table 3, the interatomic distance between the carbon of CO and the active surface oxygen of Ni₃/Al₂O₃ is the shortest (2.586 Å) in these catalysts. The polarized electronic structure and short distance also correlate with the high activity of Ni₃/Al₂O₃.

In the second transition state 5TS, the abstraction of surface oxygen by CO occurs to generate CO₂, which is the rate-determining step in all of these four single-atom catalysts. To clarify the reason why Fe₄/Al₂O₃ and Co₄/Al₂O₃ have large energy barriers, we examined the structure of intermediate 4. As presented in Table 4, the Bader charge analysis showed that both charge polarization of CO and charge transfer from adsorbate CO to the lattice O occur at intermediate 4, which reveals the large binding energy of newly formed C–Oₐₕₜₜ bond. In the case of Ni₃/Al₂O₃, the C and Oₐₜₜₜ charges are $+1.479 \, |e|$ and $-1.362 \, |e|$, respectively, for which charge polarization is larger than M=Fe and Co, but comparable to M=Pd. Also, the large negative charge of the Oₐₜₜₜ in Ni₃/Al₂O₃ and Pd₄/Al₂O₃ suggests that the charge transfer from the Oₐₜₜₜ to Ni and Pd is small and thereby the Ni–Oₐₜₜₜ interaction is weak compared to Fe₄/Al₂O₃ and Co₄/Al₂O₃. The same holds true for charge transfer as seen in charge of CO; charges of CO for M=Pd and Ni (+0.453 |e| and +0.434 |e|) are larger than those for M=Fe and Co (+0.230 |e| and +0.362 |e|). Short bond distances of the newly formed C–Oₐₜₜₜ bonds in Pd₄/Al₂O₃ and Ni₃/Al₂O₃ also confirm the large binding energy, which is consistent with the occupied O-p orbital closer to the Fermi level in Pd₄/Al₂O₃ and Ni₃/Al₂O₃ than in Fe₄/Al₂O₃ and Co₄/Al₂O₃. The above discussion reveals that charge polarization of CO, charge transfer from Oₐₜₜₜ to M and from CO to surface, as well as the structure of the CO-adsorbed surface, are important factors for the catalysis.

As depicted in Figure 6, the energy barrier of 5TS has a correlation with the reaction energy of step (2) (Equation (4)). Because the reaction energy is parallel to the energy barrier, the energy barrier can also be explained based on the stability of 6: the larger the reaction energy, the higher the energy barrier. The detailed examination of 5TS revealed that the distances between the metal and the carbon atom are 2.324, 2.669, 2.624, and 1.852 Å, respectively, for M₄/Al₂O₃ (M=Pd, Fe, Co, and Ni), indicating that the transition state is late for Fe₄/Al₂O₃ and Co₄/Al₂O₃, which is in agreement with their high energy barriers.

The adsorption energy of O2 at O-vacancy for four catalysts in step (3) (Equation (5)) is correlated to the binding energy of the doped metal atom; the O2 adsorption energy of M₄/Al₂O₃ follows the same order as the binding energy $E_b$ in Table 1. The order of the first and second CO adsorption energies, BE(1) and BE(3), for M₄/Al₂O₃ (M=Pd, Fe, Co, and Ni) is the same, although BE(3) is much smaller than BE(1). The calculations showed that the Bader charge of M in intermediate 8 is smaller than that in reactant 1 (Table S7), revealing that the interaction of the lone pair electrons of CO with the metal atom becomes weak in intermediate 9, which is consistent with the low values of BE(3). The PDOS of s and d orbitals of the metal atom in intermediate 8 is shown in Figure S10. It is found that for M₄/Al₂O₃ (M=Pd, Co, and Ni), there are obvious occupied and unoccupied s and d orbitals close to the Fermi level. In contrast, there is no evident PDOS of occupied s and d orbitals near the Fermi level in the case of Fe₄/Al₂O₃, resulting in the weak adsorption energy of the second CO for Fe₄/Al₂O₃.

In intermediate 9, the O–O bond distance of pre-adsorbed O2 ranges from 1.423 to 1.450 Å, which is much longer than the bond distance (1.236 Å) of the gas-phase oxygen molecule. In particular, the O–O bond distance of Ni₃/Al₂O₃ is the longest in these catalysts (Table S9), revealing that adsorbed oxygen is
most activated by the Ni/Al₂O₃ catalyst and that it reacts preferentially with the adsorbed CO. Using PDOS, we found the relevant orbital hybridization between O-π orbitals and M-ð orbitals in both spin-up and spin-down channels for all four catalysts (Figure S11), similarly to the observation on single-atom catalysts Mₓ/FeOₓ (M = Pt, Rh, and Pd).⁹ Albeit there are unoccupied O-π orbitals near Fermi level for all Mₓ/Al₂O₃ (M = Pd, Fe, Co, and Ni), Fe/Al₂O₃ does not have active occupied O-π orbitals above ~1.0 eV, which leads to the relatively high energy barrier in Fe/Al₂O₃. The Bader charge analysis also showed that the carbon atom and active oxygen atom in Niₓ/Al₂O₃ are evidently positively and negatively charged, respectively, which would result in the low energy barrier at 10TS.

In the catalytic cycle, Niₓ/Al₂O₃ and Pdₓ/Al₂O₃ keep a spin state of M = 1 (doublet), whereas the spin states of Feₓ/γ-Al₂O₃ and Coₓ/γ-Al₂O₃ change. This can be attributed to the coordination property of Fe and Co. For example, on adsorption of the first CO molecule on the Coₓ/γ-Al₂O₃, the spin state changes from M = 4 (quintet) to M = 0 (antiferromagnetic singlet) (Figures S2 and S4), indicating that Co strongly binds to CO. This result is consistent with the large adsorption energy of CO on Coₓ/γ-Al₂O₃. On the other side, for the other three catalysts, the spin state does not change after CO adsorption. The constant spin state of Niₓ/Al₂O₃ and Pdₓ/Al₂O₃ also reveals that adsorbed molecules such as CO and OCO adsorb on catalysts. Under the MvK mechanism, the rate-determining step of the CO oxidation by all these heterogeneous single-atom catalysts is the abstraction of surface oxygen by CO to generate the first CO₂ molecule. The origin of the low-energy barrier for Niₓ/Al₂O₃ was investigated by analyzing electronic structures and geometries of intermediates and transition states, and PDOS. The PDOS of O-π near the Fermi level, CO-adsorbed surface structure, charge polarization of CO and charge transfer from CO to surface are important factors for the catalysis; Niₓ/Al₂O₃ satisfies all these factors. As a result of the low binding energy of Pd and Ni, the neighboring O atom is weakly bound to Pd or Ni and therefore becomes highly active toward CO, which leads to their enhanced catalytic performance. Hereby we wish to recommend the use of metals with a stable +II oxidation state for the construction of good catalysts.

**Computational Section**

The 2 x 1 supercell model (11.17 x 8.41 Å)⁹⁴ of the dehydrated γ-Al₂O₃(100) consists of eight atomic layers, of which the top five atomic layers are allowed to relax in the calculations while the bottom three are fixed, as shown in Figure 1. With these choices, the computational slab of dehydrated γ-Al₂O₃(100) contains 100 atoms. A vacuum spacing of 15 Å was added in the z-direction without a dipole correction to avoid the interaction between the slab and its repeated motif. The lattice parameters were fixed in optimizations. Test calculations with a 2 x 2 supercell model showed that incrementing the model size has little influence on the adsorption energy. All spin-polarized DFT calculations were performed by employing the Vienna Ab Initio Simulation Package (VASP).⁹⁵ The generalized-gradient approximation in the form of PBE⁹⁶ was used as the correlation and exchange energy functional, which has been widely used in previous DFT calculations of single-atom catalysts.⁹⁷-⁹⁹ To describe the interactions between valence electrons and the ion core, the projector augmented wave (PAW) method was adopted.⁹⁵ The kinetic cut-off energy for the plane wave basis set for valence electrons was fixed at 400 eV. We also used the Gaussian broadening method with a smearing width of 0.05 eV to improve convergence of states near the Fermi level. A 2 x 2 x 1 Monkhorst-Pack mesh⁹⁶ was used to sample the first Brillouin zone. Test calculations with a 3 x 3 x 1 Monkhorst-Pack mesh gave similar results. The convergence criteria for the electronic structure and geometry optimization were 10⁻⁵ eV and 0.02 eV Å⁻¹, respectively. The calculations of isolated small molecules were performed by using a (10 Å x 10 Å x 10 Å) unit cell with the Γ-point only for the k-point sampling. To locate transition states (TSs), we used the climbing-image nudged elastic band (CI-NEB) method⁹⁸,⁹⁹ in which at least five images were used. Geometry optimizations of TSs were conducted until the forces on each free atom in TSs were less than 0.05 eV Å⁻¹. For Bader charge analysis, the program developed by the Henkelman group was used.⁹⁵

**Conclusions**

By using density functional theory calculations of slab model, we performed a comprehensive theoretical investigation on a series of single-atom catalysts Mₓ/γ-Al₂O₃ with ubiquitous elements such as Fe, Co, and Ni. Our results suggest that, among these systems, Niₓ/Al₂O₃ catalyst is more active than the recently reported Pdₓ/Al₂O₃, with regard to the low-temperature CO oxidation, as a result of its significantly lower energy barriers in the catalytic cycle. On the other hand, Feₓ/Al₂O₃ and Coₓ/Al₂O₃ have a higher energy barrier and, therefore, are less effective as catalysts. Under the MvK mechanism, the rate-determining step of the CO oxidation by all these heterogeneous single-atom catalysts is the abstraction of surface oxygen by CO to generate the first CO₂ molecule. The origin of the low-energy barrier for Niₓ/Al₂O₃ was investigated by analyzing electronic structures and geometries of intermediates and transition states, and PDOS. The PDOS of O-π near the Fermi level, CO-adsorbed surface structure, charge polarization of CO and charge transfer from CO to surface are important factors for the catalysis; Niₓ/Al₂O₃ satisfies all these factors. As a result of the low binding energy of Pd and Ni, the neighboring O atom is weakly bound to Pd or Ni and therefore becomes highly active toward CO, which leads to their enhanced catalytic performance. Hereby we wish to recommend the use of metals with a stable +II oxidation state for the construction of good catalysts.
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Conflict of interest

The authors declare no conflict of interest.

Keywords: CO oxidation · density functional theory · heterogeneous catalysis · single-atom catalyst · structure–activity relationships

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