MODELING HOT GAS FLOW IN THE LOW-LUMINOSITY ACTIVE GALACTIC NUCLEUS OF NGC 3115

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ABSTRACT

Based on the dynamical black hole (BH) mass estimates, NGC 3115 hosts the closest billion solar mass BH. Deep studies of the center revealed a very underluminous active galactic nucleus (AGN) immersed in an old massive nuclear star cluster. Recent 1 Ms Chandra X-ray visionary project observations of the NGC 3115 nucleus resolved hot tenuous gas, which fuels the AGN. In this paper we connect the processes in the nuclear star cluster with the feeding of the supermassive BH. We model the hot gas flow sustained by the injection of matter and energy from the stars and supernova explosions. We incorporate electron heat conduction as the small-scale feedback mechanism, the gravitational pull of the stellar mass, cooling, and Coulomb collisions. Fitting simulated X-ray emission to the spatially and spectrally resolved observed data, we find the best-fitting solutions with \( \chi^2 / \text{dof} = 1.00 \) for \( \text{dof} = 236 \) both with and without conduction. The radial modeling favors a low BH mass \( \lesssim 1.3 \times 10^9 \, M_\odot \). The best-fitting supernova rate and the best-fitting mass injection rate are consistent with their expected values. The stagnation point is at \( r_\text{st} \lesssim 1'' \), so that most of the gas, including the gas at a Bondi radius \( r_B = 2''-4'' \), outflows from the region. We put an upper limit on the accretion rate at \( 2 \times 10^{-3} \, M_\odot \, \text{yr}^{-1} \). We find a shallow density profile \( n \propto r^{-\beta} \) with \( \beta \approx 1 \) over a large dynamic range. This density profile is determined in the feeding region \( 0.5-10'' \) as an interplay of four processes and effects: (1) the radius-dependent mass injection, (2) the effect of the galactic gravitational potential, (3) the accretion flow onset at \( r \lesssim 1'' \), and (4) the outflow at \( r \gtrsim 1'' \). The gas temperature is close to the virial temperature \( T_v \) at any radius.

Key words: accretion, accretion disks – black hole physics – galaxies: individual (NGC 3115) – galaxies: nuclei – hydrodynamics – stars: winds, outflows

Online-only material: color figures

1. INTRODUCTION

Both theory and observations indicate that a typical active galactic nucleus (AGN) is not particularly active (Ho 2008). A median Eddington ratio of \( \lambda = L_{\text{bol}}/L_{\text{Edd}} \sim 10^{-5} \) is found in a distance-limited Palomar survey of the nearby AGNs (Ho 2009), so that most galactic nuclei are inactive at any given time and any given nucleus is inactive most of the time. The observed short AGN duty cycle (Greene & Ho 2007) is readily explained by the large-scale feedback shutting off the central engine soon after an active phase begins (Hopkins & Hernquist 2009) leading to the so-called low-luminosity (LL) AGN.

The theory of the gas flow in LLAGNs has been studied for over 60 yr. In their seminal work Bondi (1952) introduced a characteristic radius of the black hole (BH) gravitational influence now called the Bondi radius \( r_B = 2 G M_{\text{BH}} / c_s^2 \), where \( c_s \) is the adiabatic sound speed. Since then BH feeding is traditionally associated with processes near the Bondi radius. It was uncovered over the years that the Bondi model has a limited applicability to LLAGNs. Quataert & Narayan (2000) showed that there may exist a smooth transition at \( r \sim r_B \) from the galactic flow to the accretion flow governed by a transition from the galactic gravitational potential to the BH potential. Shcherbakov & Baganoff (2010) showed that the gas starting at the Bondi radius may not settle into an inflow, but instead be a part of an outflow. Various models were proposed for the inflow such as advection-dominated accretion flows (ADAFs; Narayan & Yi 1995), convection-dominated accretion flows (CDAFs; Narayan et al. 2000; Quataert & Gruzinov 2000), and adiabatic inflow–outflow solutions (ADIoS; Blandford & Begelman 1999).

LLAGNs are fed via a variety of the mechanisms. First, the gas traveling from galactic scales may form an inflow onto the BH (Hopkins & Hernquist 2006). Galaxies with a large gas content such as our own spiral galaxy may feed this way (Czerny et al. 2013). On the other hand, elliptical galaxies typically lack a substantial inflow owing to a small gas content and low cooling efficiency (Mathews & Brighenti 2003). Their nuclear star clusters may take over the feeding. The stars shed mass in amounts often large enough to sustain the observed level of AGN activity (Holzer & Axford 1970; Ciotti & Ostriker 2001; Quataert 2004; Hopkins & Hernquist 2006; Ciotti & Ostriker 2007; Cuadra et al. 2008; Ho 2009; Volonteri et al. 2011; Miller et al. 2012), Tidal disruptions (Milosavljević et al. 2006; MacLeod et al. 2012), consecutive partial disruptions (MacLeod et al. 2013), and stellar collisions (Freitag & Benz 2002) account for a small fraction of LLAGN activity, so we ignore such mechanisms. Collisions of ejected stellar winds in the feeding region at \( r \sim r_B \) produce hot gas with a temperature up to \( 10^7 \, K \) (Lamers & Cassinelli 1999; Quataert 2004; Cuadra et al. 2008). The tenuous gas does not cool, but maintains the virial temperature \( T_v \sim 0.3-1 \, \text{keV} \) and radiates mostly in X-rays. Thus, X-ray studies of LLAGN feeding are warranted.

X-ray studies of nearby LLAGNs include several large Chandra projects: an X-ray visionary project (XVP) for Sgr A* (PIs: Baganoff, Markoff, and Nowak; Wang et al. 2013), an XVP for NGC 3115 (PI: Irwin; Wong et al. 2014), and AMUSE surveys (PIs: Gallo and Treu; Miller et al. 2012). The unparalleled X-ray spatial resolution of the Chandra satellite allows for the study in unprecedented detail of the gas flow within the...
BH Bondi radius in several nearby galaxies such as M31, M87, the Milky Way, and NGC 3115 (Garcia et al. 2010). Here we focus on NGC 3115, which has an accumulated exposure of 1 Ms during the year 2012 with the ACIS-S instrument onboard Chandra. NGC 3115 is an S0 lenticular galaxy at a distance of about $d = 9.7$ Mpc (Tonry et al. 2001). It hosts a supermassive BH with mass $M_{\text{BH}} \geq 10^9 M_\odot$ (Kormendy et al. 1996; Emsellem et al. 1999). Despite the galaxy being viewed edge-on, the hydrogen column density $N_H$ toward its center is consistent with the local Milky Way $N_H$ (Wong et al. 2011, 2014). Cold gas is practically absent near the center of NGC 3115. The nucleus has a Bondi radius of $r_B = 2''-4''$, which is readily resolved with Chandra. The AGN was only recently found in NGC 3115 owing to radio observations (Wrobel & Nyland 2012). Source radio luminosity is $\nu L_\nu(8.5\text{GHz}) = 3.1 \times 10^{35} \text{erg s}^{-1}$. The nuclear star cluster was extensively observed in the optical band in search of a supermassive BH with both ground-based instruments (Kormendy & Richstone 1992) and the Hubble Space Telescope (Kormendy et al. 1996; Emsellem et al. 1999).

The models to study LLAGN feeding have various degrees of complexity. Basic one-zone estimates are typically performed in conjunction with observational studies to relate the properties of the nuclear star clusters and the observed X-ray emission (Soria et al. 2006a, 2006b; Hopkins & Hernquist 2006; Ho 2009; Miller et al. 2012; Volonteri et al. 2011). A more self-consistent approach is to perform radius-dependent modeling. The required radial structure of both the nuclear star clusters and the X-ray emission are available, e.g., for NGC 3115. The radial modeling can quantitatively include a variety of physical effects such as the mass and the energy injection, conduction, and the galactic gravitational potential. The system of equations can be defined and solved in search for physical solutions (Quataert 2004; Shcherbakov & Baganoff 2010) encompassing a huge dynamic range of $\sim 10^6$ from the event horizon to far beyond the Bondi radius. The disadvantages of radial modeling include approximations for vertical flow structure and the inability to properly deal with the turbulent inhomogeneous medium. The numerical simulations of the LLAGN feeding allow for the proper treatment of cooling (Gaspari et al. 2013), feedback (Guo & Mathews 2013), and outflows (Yuan et al. 2012b, 2012a). However, full numerical simulations are computationally expensive, which limits the dynamic range and the number of runs to explore the range of inputs (Yuan et al. 2012b; Sadowski et al. 2013). In the present paper we adopt radial modeling, which allows us to compute many solutions and fit the X-ray data in a more consistent way compared to the one-zone estimates. Our results help to illuminate the relative importance of various physical effects and define the relevant ranges of model parameters such as the BH mass. Our computations provide the starting point for future numerical simulations of NGC 3115 and other LLAGNs.

The development of such radial gas flow models for NGC 3115 and fitting the X-ray XVP data are the topics of this manuscript. In Section 2 we present the properties of the nuclear star cluster in NGC 3115. We quantify the mass loss by stars, the energy injection by the stellar winds and supernovae, and the angular momentum injection. In Section 3 we explore the various effects and features of gas dynamics and devise a radial system of dynamical equations. We include conduction, the gravitational pull by the enclosed stellar mass, cooling, and the collisional coupling of the ions and the electrons. In Section 4 we outline the procedure of computing radiation from the dynamical gas model and fitting the X-ray data. We perform optically thin radiative transfer with up-to-date collisional ionization equilibrium (CIE) plasma emissivity and do the radius-resolved spectroscopy. In Section 5 we present the best-fitting conductive and advective solutions. We achieve acceptable fits with $\chi^2 / \text{dof} = 1.00$, which indicates the sufficiency of the radial models. However, we identify room for improvement as prompted by the fit residuals. In Section 6 we discuss the results and provide conclusions. The density is found to behave approximately as $n \propto r^{-1}$ over a large dynamic range and across the Bondi radius. We discuss multiple reasons for this density slope. We identify the limitations of the presented models and discuss directions of future research. The methods of the paper are visualized in Figure 1.

2. PROPERTIES OF NUCLEAR STAR CLUSTER

The first step to understand LLAGN feeding is to quantify the properties of nuclear star clusters, which provide matter, energy, angular momentum, and enclosed mass. Nuclear star clusters are ubiquitously present near supermassive BHs (Milosavljević 2004; Soria et al. 2006b; Seth et al. 2008; Graham & Spitler 2009; Genzel et al. 2010). The matter, which the cluster stars shed, often constitutes most of the AGN fuel (Ho 2009). Luckily, large amounts of data are available on nuclear star clusters as the by-products of weighing their supermassive BHs, e.g., by the Nuker group (PI: Richstone; Kormendy & Richstone 1995; Kormendy & Gebhardt 2001). The nucleus of NGC 3115 is one of the most studied. We use the data from earlier ground-based observations by Kormendy & Richstone (1992), who modeled the deprojected luminosity and the enclosed mass profiles. Later Hubble data showed general agreement with those earlier observations (Emsellem et al. 1999).

2.1. Enclosed Mass

A direct by-product of measuring the velocity dispersion is the radial profile of the enclosed mass (Kormendy & Richstone 1992). As the surface brightness profile is determined and deprojected, the mass-to-light $M/L$ ratio for the $V$-band is computed at each radius. A constant value $M/L_V = 4.0$ is reached far from the BH, despite the fact that the ratio $M/L_V$ varies close to the BH between different models of the velocity and the mass distributions. Neglecting any gradient in the stellar mass function, we assume a constant $M/L_V = 4.0$ ratio for the enclosed stellar mass at any radius. Then we multiply the deprojected luminosity profile for the best-fitting D3 stellar dynamic model in Kormendy & Richstone (1992) by the $M/L_V$ ratio and find the enclosed stellar mass. Direct inference of the enclosed stellar mass from the velocity dispersion is unreliable near the BH, when the BH mass is not precisely known. Setting a constant stellar $M/L_V$ allows to disentangle the BH mass from the stellar mass. In the bottom panel of Figure 2 we show the computed stellar enclosed mass $M_{\text{enc}}$ (solid line) and the total enclosed mass calculated in Kormendy & Richstone (1992) (dashed line).

2.2. Mass Injection

The most important feature of nuclear star clusters is the ability to inject matter, often in the form of stellar winds, to fuel the supermassive BHs. Many theoretical and observational studies of the matter injection rates and their relation to the observed quantities were conducted over the years (see Ho 2009 for a review). The mass loss rate is found to be
Figure 1. Modeling the hot gas flow onto the supermassive BH in the NGC 3115 nucleus. The gas is injected in the feeding region at \( r = r_B \) by the stars. Supernovae dominate the energy input in the outer flow \( r \gtrsim 1'' \), while the collisions of stellar winds dominate the energy input in the inner flow \( r \lesssim 1'' \). Most of the gas outflows from the feeding region, while a fraction of the gas accretes. The extended gas emission is observed in the NGC 3115 nucleus with Chandra with the XVP observation (PI: Irwin) and is described in a companion paper (Wong et al. 2014). We construct radial inflow–outflow solutions for the gas and fit the radius-resolved spectra with simulated spectra. We find an indication of a low BH mass \( M_{BH} \approx 1.3 \times 10^6 M_{\odot} \) and estimate the mass injection rate normalization, the energy injection rate, and the stagnation point location. The tick marks, which denote the distance from the BH, are drawn out of proportion. The image of the Chandra satellite: copyright NGST.

(A color version of this figure is available in the online journal.)

the formulas (1) and (2) agree for NGC 3115 to within a factor of two. These formulas are equivalent for a constant adopted \( M/L_V \) ratio, and we use the latter one for convenience. We compute the profile of \( M_\ast \) from the deprojected \( V \)-band luminosity given by the best-fitting model D3 in Kormendy & Richstone (1992).

We present the resultant mass loss rate in the top panel of Figure 2. While the mass loss rate per unit volume sharply rises toward the center, the depicted contribution per unit radius drops inward. The area under the curve is the total mass injection rate. For the modeling of gas dynamics we normalize the mass loss rate by a radius-independent free parameter on the order unity \( f_q \sim 1 \).

2.3. Energy Injection

Several heating mechanisms with comparable power inputs operate in nuclear star clusters. First, when the mass loss is accomplished via stellar winds, those winds deposit their kinetic energy into the medium. The collisions of winds turn that kinetic energy into heat. Nuclear star clusters with young stellar populations, such as the one in our Galactic center, produce winds with high velocities up to \( 2000 \text{ km s}^{-1} \) from Wolf–Rayet and other young stars (Cuadra et al. 2008). However, old stellar populations mostly shed matter and produce winds from asymptotic giant branch (AGB) stars (Vassiliadis & Wood 1993; Hurley et al. 2000; Groenewegen et al. 2007) with a correspondent wind velocity under \( 50 \text{ km s}^{-1} \) (Knapp et al. 1982; Marengo 2009; Libert et al. 2010; Leitner & Kravtsov 2011). We use the terms “stellar winds” and “mass lost by stars.”

proportional to the stellar mass and to the stellar luminosity. The proportionality coefficients depend on the stellar population age \( t \). The correlation with stellar mass based on the stellar evolution models is summarized in Jungwiert et al. (2001). Their proposed formula reads

\[
\frac{M_\ast}{M_i} \approx \frac{0.055}{t + t_0}
\]

for solar stellar metallicity. Here \( M_i \) is the initial stellar mass and \( t_0 = 5 \text{ Myr} \). We estimate the stellar age in the nucleus of NGC 3115 with the stellar evolution code EzGal (Mancone & Gonzalez 2012). We run the simple stellar population models of Bruzual & Charlot (2003) and Conroy et al. (2009); Conroy & Gunn (2010) for solar metallicity and reach the observed ratio \( M/L_V = 4.0 \) for the age \( t \sim 5 \text{ Gyr} \) indicative of an old stellar population. At that age the stellar mass is \( M_\ast \approx 0.62 M_i \) (Jungwiert et al. 2001) and the stellar mass loss rate is \( \dot{M}_\ast = 1.8 \times 10^{-11} M_\odot \text{ yr}^{-1} \). We also discuss the gas and the stellar metallicities in Section 2.5 below.

Another method to determine the stellar mass loss rate is from the correlation with the source luminosity. The mass loss rate \( M_\ast \) is proportional to the \( V \)-band luminosity as

\[
\dot{M}_\ast \approx 3 \times 10^{-11} \left( \frac{L_V}{L_\odot, V} \right) M_\odot \text{ yr}^{-1}
\]

for an old stellar population Faber & Gallagher (1976); Padovani & Matteucci (1993). The normalization coefficient is known to within a factor of two (Ho 2009). A similar relation exists between the \( M_\ast \) and the \( B \)-band luminosity (Ciotti et al. 1991; Athey et al. 2002). The normalizations determined by
The relative stellar motions is on the order of the stellar velocity field of the BH and the enclosed stellar mass. The velocity of exchangeable mass loss rate in stellar winds.

The energy imparted into the stellar winds by the relative stellar motions and

interchangeably, while having in mind that AGB stars shed mass also via planetary nebulae.

The mass-shedding stars move in a combined gravitational field of the BH and the enclosed stellar mass. The velocity of the relative stellar motions is on the order of the stellar velocity dispersion \( \sigma \), which is \( \sigma \sim 300 \text{ km s}^{-1} \) in the NGC 3115 nucleus (Kormendy & Richstone 1992). Then the relative stellar motions introduce much more energy than the motions of matter with respect to the injecting stars (Hillel & Soker 2013), and the latter is ignored. For the purpose of the gas dynamical modeling we use the effective stellar wind velocity

\[
v_{w,\text{eff}} = \sqrt{v_{w,\text{SN}}^2 + v_{w,\text{SN}}^2} = \left( \frac{c^2 r g M_{\text{enc}} + M_{\text{BH}}}{M_{\text{BH}}} + v_{w,\text{SN}}^2 \right)^{1/2}.
\]

The supernova energy injection rate is equivalent to the energy injection rate of

Another important energy source are supernovae explosions. According to Mannucci et al. (2005) the supernova rate in S0 galaxies (like NGC 3115) is \( R_{\text{SN}} \sim 4 \times 10^{-11} M_\odot/\text{yr} \). Supernovae Type Ia occur in such galaxies more frequently than other kinds due to the large stellar population age. Each supernova is typically assumed to inject \( E_K = 10^{51} \text{ erg of useful energy} \) (Benson 2010) into the gas, while the typical ejecta mass is \( M_\text{ej} \sim 1.5 M_\odot \) for the Type Ia (Nauenberg 1972). Then the specific mass injection rate is \( \sim 10^{-13} \text{ yr}^{-1} \). The specific mass injection rate in stellar winds is \( \sim 10^{-11} \text{ yr}^{-1} \), so that supernovae inject a negligible amount of mass. The specific energy injection rate in stellar winds is \( \sim 10^{37} \text{ erg yr}^{-1} M_\odot^{-1} \) for a typical velocity

\( v_{w,\text{SN}} \sim 300 \text{ km s}^{-1} \). The specific energy injection rate in supernovae is \( \sim 4 \times 10^{37} \text{ erg yr}^{-1} M_\odot^{-1} \). The supernovae inject more energy than provided by stellar winds.

An important question is whether the energy injection by supernovae may be averaged over the characteristic gas flow timescale. Since a mass of about \( 10^{10} M_\odot \) resides at the Bondi radius, one supernova should happen there every \( t_{\text{SN}} \sim 2.5 \times 10^5 \text{ yr} \). However, the sound crossing time is \( t_s \sim 10^6 \text{ yr} \). Then about 400 supernovae happen before the system reacts, so we treat the energy injection from the supernovae on average. A more detailed a posteriori justification is given in Section 6.

Some energy is contributed into the feeding region by accreting objects such as low-mass X-ray binaries (LMXBs). We estimate the mechanical energy output \( L_{\text{mech}} \) of the accreting objects by equating it to their X-ray luminosity \( L_X = L_X \), which is a natural assumption for the most powerful high efficiency systems. Knowing that \( \sim 10^7 \) photons came from the LMXBs over 1 Ms Chandra observation, we estimate their X-ray luminosity to be \( L_X \sim 4 \times 10^{38} \text{ erg s}^{-1} \). Then the mechanical luminosity per unit mass is \( L_{\text{mech}} \sim 10^{36} \text{ erg yr}^{-1} M_\odot^{-1} \) for a stellar mass of \( 10^{10} M_\odot \), which is an order of magnitude lower than the energy injection rate in supernovae or stellar winds. We neglect the energy contribution of the LMXBs.

In sum, the two dominant energy contributors are supernovae and colliding stellar winds. The specific energy injection rate is constant for the supernovae and is a strong function of radius for the colliding stellar winds. The supernova heating power is equivalent to the power of the colliding stellar winds with a velocity \( v_{w,\text{SN}} \sim 500 \text{ km s}^{-1} \), which we call an effective supernova wind velocity. We combine the energy inputs into a total effective wind velocity as

\[
v_w = \sqrt{v_{w,\text{SN}}^2 + v_{w,\text{SN}}^2} = \left( \frac{c^2 r g M_{\text{enc}} + M_{\text{BH}}}{M_{\text{BH}}} + v_{w,\text{SN}}^2 \right)^{1/2}.
\]

In the middle panel of Figure 2 we plot \( v_w \) for the fiducial \( v_{w,\text{SN}} = 500 \text{ km s}^{-1} \) (solid line) and \( v_w \) for the same effective supernova contribution, but for the zero enclosed stellar mass \( M_{\text{enc}} = 0 \) (dashed line). In the modeling we leave the effective supernova wind velocity to be a free parameter, but check the best-fitting value of \( v_{w,\text{SN}} \) for consistency.

![Figure 2](https://example.com/figure2.png)

Figure 2. Radial profiles of the quantities in the NGC 3115 nuclear star cluster: the mass loss rate \( dM/dr \) in the upper panel, the effective wind velocity \( v_w \), the enclosed mass \( M_{\text{enc}} \) in the bottom panel. The area under the curve in the upper panel gives the total mass injection rate \( M_{\text{inj}} \).
2.4. Angular Momentum Injection

The NGC 3115 nuclear star cluster possesses a non-zero mean rotation. In their paper Kormendy & Richstone (1992) report the velocity profiles along the semi-major and semi-minor axes of the galaxy, which is viewed almost edge-on. The mean rotation is absent along the semi-minor axis, while the mean angular velocity measured along the semi-major axes reaches more than 200 km s$^{-1}$. In the top panel of Figure 3 we show the radial profile of the mean rotational velocity $v_{\phi}$ from Kormendy & Richstone (1992). We fit the data points with the power-law

$$v_{\phi} = 257 \left( \frac{r}{20''} \right)^{0.287} \text{km s}^{-1},$$

which quickly approaches zero at a small radius. In the bottom panel of Figure 3 we show the circularization radius $r_{\text{circ}}$ as a function of the injection radius $r$ (solid line) given as a solution of the equation

$$r_{\text{circ}} v_{K} (r_{\text{circ}}) = r v_{\phi}(r),$$

where the Keplerian velocity is computed in the joint gravitational potential. The dashed line given by the equation $r_{\text{circ}} = r$ represents the injection with the Keplerian angular velocity $v_{\phi} = v_{K}$. The presented radial dependence of the angular velocity qualitatively agrees with the transition to a rotationally supported galactic disk at a large radius and with the transition to purely random stellar motions at a small radius.

2.5. Gas Metallicity

It is difficult to determine the gas metallicities. The stars in the NGC 3115 off-nuclear star clusters have sub-solar metallicity [Fe/H] $\approx -0.5$ close to the center (Arnold et al. 2011). However, the stellar metallicity might not be a good proxy for the gas metallicity (Su & Irwin 2013). The gas metallicity is higher, since only the evolved stars with a large fraction of the heavy elements eject the substantial amounts of mass. Still, the stellar mass loss rate does not strongly depend on the stellar metallicity of AGB stars (Marigo & Girardi 2007; Weiss & Ferguson 2009). Since the sound crossing time of the feeding region is only about $t_s \sim 10^9$ yr, the gas metallicity reflects the metallicity of the recently ejected mass.

While the metallicity of the hot gas in NGC 3115 cannot be easily measured (Wong et al. 2014), the metallicity of the cooler gas is measured in many other galactic nuclei to be solar or supersolar (Storchi Bergmann & Pastoriza 1989; Hamann et al. 2002). Relatively few examples exist with sub-solar gas metallicity (Groves et al. 2006). Super-solar metallicity is also favored for the cool absorbing gas near Sgr A$^*$ in our Galactic center (Wang et al. 2013). With the absence of a better estimate we fix the gas metallicity in NGC 3115 at the solar value $Z/Z_\odot = 1$. This approximation is not restrictive. As we discuss in Wong et al. (2014), the gas metallicity is strongly degenerate with the density normalization. Since most of the X-rays are emitted in the metal lines, the gas density is inversely proportional to the assumed gas metallicity to preserve the constant density of metals.

3. GAS DYNAMICS

In Section 2 we characterized the gas injected into the BH feeding region. In this section we elaborate on the physical laws, which govern the gas dynamics. We first describe the distinct effects and then present a full set of radial equations.

3.1. Physical Effects

3.1.1. Conduction and Small-scale Feedback

Since the early introduction of ADAFs (Bondi 1952; Narayan & Yi 1995), several effects were shown to break the advective nature of the hot radiatively inefficient accretion flows and result in a shallow density profile $n \propto r^{-\beta}$ with $\beta = 0.5$–1.0, while $\beta = 1.5$ for ADAFs. The flow is not advective, when the energy from the hotter inner flow is deposited into the cooler outer flow, which leads to a super-virial gas temperature. It immediately follows from the pressure balance equation

$$\frac{1}{n} \frac{\partial p}{\partial r} = \frac{\partial (nk_BT)}{\partial r} = -\frac{G M_{\text{BH}}}{r^2},$$

that in the absence of the source terms that a higher temperature $T$ leads to a shallower density slope $\beta$.

We employ the term “small-scale feedback” for such energy transfer from the inner flow to the outer flow in an analogy with large-scale feedback, when the central AGN influences the entire galaxy (Begelman & Nath 2005; Di Matteo et al. 2005; Silk & Ninster 2010). The two main small-scale feedback processes are convection and conduction. Convection was shown to be important in collisional flows (Narayan et al. 2000; Quataert & Gruzinov 2000). Electron heat conduction appears to dominate convection in collisionless flows (Shcherbakov & Baganoff 2010). No heat is transferred via conduction across magnetic field lines, but the effective conductivity is still high in the
turbulent flows as proposed theoretically (Narayan & Medvedev 2001) and confirmed with numerical simulations (Parrish et al. 2010). The action of conduction helps to explain the shallow density slope of the Sgr A* accretion flow (Johnson & Quataert 2007; Shcherbakov & Baganoff 2010).

Outflows may lead to the shallow density profile as well (Yuan et al. 2003). However, it might be non-trivial to disentangle outflows from small-scale feedback. The simulations by Yuan et al. (2012a, 2012b) showed both outflows above and below the midplane and convection in the equatorial plane. Small-scale feedback may help to launch the outflows. When convection or conduction transports energy outward near the equatorial plane, outflows are more easily launched above and below the midplane facilitated by the higher gas temperature. Such a mechanism is distinct from ADIOS (Blandford & Begelman 1999), which is based on outflows in the absence of small-scale feedback. Modeling the flow in one dimension, we do not distinguish between small-scale feedback and outflows. For the effective combined action of these effects we choose, following Shcherbakov & Baganoff (2010), unsaturated conduction with the flux proportional to the temperature gradient \( F_{\text{cond}} \propto dT/dr \) with collisionless conductivity

\[
\kappa = 0.1\sqrt{k_B T_e/m_p n}. \tag{8}
\]

The outer flow in NGC 3115 is marginally collisional with a mean free path \( r_{\text{mfp}} \sim 0.01r_B \) at the Bondi radius. However, as we show below, heat conduction effect is subdominant in the feeding region. The mean free path becomes equal to the radius at \( r = r_{\text{mfp}} \approx 0.1 \), where conduction becomes dynamically important. Thus, the solutions computed with high conductivity are physical, and we employ conductivity given by the formula (8) at any radius. The prescriptions with a lower conductivity in the outer flow reduce the stability of the numerical algorithm, and are avoided. To test the importance of small-scale feedback, we compute the flow models with and without conduction.

3.1.2. Gravitational Pull by the Enclosed Stellar Mass

The accretion flows governed by the BH gravity often smoothly connect to the galactic flows governed by the gravity of the enclosed mass (Quataert & Narayan 2000). According to Figure 2, the enclosed stellar mass in the NGC 3115 nucleus exceeds the BH mass at about \( r_s \approx 1'' \), which is less than the Bondi radius \( r_s \lesssim r_B \). Then, unlike in the Bondi model, constant temperature and constant density are not expected outside of \( r_B \). Outflows need more energy to escape the additional gravitational pull. The gas not bound to the BH may appear bound to the surrounding stellar mass.

3.1.3. Cooling

Cooling is another effect important for AGN feeding. Cool gas readily rushes onto the BH, as it does not have enough pressure to counteract the gravity. An inverted shape of the cooling curve supports a runaway catastrophe, as the gas loses energy slowly at \( T \sim 10^6-10^7 \) K, but quickly at \( T \sim 10^8 \) K (Sutherland & Dopita 1993). The cooling power is proportional to the density squared \( P_{\text{cool}} \propto n^2 \), and the cooling timescale is inversely proportional to the density \( t_{\text{cool}} \propto n^{-1}. \) Then this effect is less pronounced in low density systems such as the LLAGNs.

Cooling may influence the accretion in our Galactic center. The marginal importance of cooling is indicated by Drappeau et al. (2013) close to the plunging region of Sgr A*. Some models of Sgr A* show runaway cooling in the feeding region (Cuadra et al. 2005), while more realistic models exhibit milder temperature drops (Cuadra et al. 2008). A setup very similar to NGC 3115 was chosen by Gaspari et al. (2013) for their numerical simulations of accretion flows. They find only a small temperature reduction for the low density gas observed in the NGC 3115 nucleus. Nevertheless, we include the effect of cooling in the dynamical modeling. We employ the CIE cooling curve from Sutherland & Dopita (1993) and ignore the effects of clumping and spatial inhomogeneity.

3.1.4. Coupling of Ions and Electrons

The thermalization time of a particle distribution in hot tenuous gas is much shorter than the energy exchange time between the electrons and the ions via Coulomb collisions (Shkarofsky et al. 1966). We follow the standard practice and consider thermal ions and thermal electrons with temperatures \( T_i \) and \( T_e \), respectively. In addition to Coulomb collisions, relatively strong collisionless effects operate at high temperature (Sharma et al. 2007). However, we only consider Coulomb collisions in the modeling in the absence of a widely accepted prescription for collisionless coupling.

3.2. Dynamical Equations

Following Shcherbakov & Baganoﬀ(2010), we solve the system of equations on the electron temperature \( T_e \), the ion temperature \( T_i \), the electron number density \( n = n_e \), and the gas radial velocity \( v_r \). The equations are modified from Shcherbakov & Baganoﬀ(2010), as we ignore the collisionless coupling of the species and the viscous conversion of the gravitational energy into thermal energy. The latter is justified, because, as we show in Section 5, the stagnation point in the best-fitting solutions is at \( r_{\text{st}} \lesssim 1'' \). Then the flow circularization radius lies within 0.05, and the viscous energy production is absent in the observed outer flow. The thermal energy production via the dissipation of the magnetic field is similarly unimportant till well within the stagnation point (Shcherbakov 2008). Two more modifications are the inclusion of cooling and the inclusion of the galactic gravitational potential. We present the full system of the dynamical equations here.

The mass balance equation is

\[
\frac{\partial n}{\partial t} + \frac{1}{r^2} \frac{\partial (n v_r r^2)}{\partial r} = f_q q(r)/\mu_{av}, \tag{9}
\]

where \( \mu_{av} \approx 1.18 \) is the average atomic mass per electron for the assumed solar metallicity. The ratio of the number of ions to the number of electrons is \( d = n_{\text{ion}}/n = 0.91 \). We consider the fully ionized species with the relative element abundances given by wilm table (Wilms et al. 2000).4 We define the mass source function \( q(r) \), such that the mass injection rate plotted in Figure 2 is \( dM_e/\partial r = 4\pi r^2 q m_p \). We normalize \( q(r) \) by the dimensionless number \( f_q \). We define the effective isothermal sound speeds

\[
c_{se} = \sqrt{\frac{k_B T_e}{m_p}} \quad \text{and} \quad c_{si} = \sqrt{\frac{k_B T_i}{m_p}}. \tag{10}
\]

4 Note, that \( \mu_{av} \) and \( d \) slightly deviate from those in Shcherbakov & Baganoﬀ(2010) due to their use of a different abundance table.
Then the Euler equation reads

\[
\frac{DV_r}{Dt} + \frac{\partial(n(c^2_r + d c^2_r))}{\partial r} + \frac{rg^2 c^2_r}{2(r-g)^2} \times \left( 1 + \frac{M_{BH}}{M_{enc}} \right) + f_q g(r) v_r = 0,
\]

where \( D/Dt = \partial/\partial t + v_r \partial/\partial r \) is the Lagrangian derivative.

The relativistic energy exchange rate per unit volume between the electrons and ions via Coulomb collisions is (Stepney & Guilbert 1983; Narayan & Yi 1995)

\[
F_{ie,rel} = \frac{3}{2} m_e^2 n_{ion} \sigma_T c \frac{k_B T_i - k_B T_e}{K_2(1/\theta_e)} K_2(1/\theta_i) \ln L
\]

\[
\times \left[ \frac{2(\theta_e + \theta_i)^2 \theta_e + \theta_i}{\theta_e + \theta_i} K_1 \left( \theta_e + \theta_i \right) + 2 K_0 \left( \theta_e + \theta_i \right) \right].
\]

where \( K_n \) is the modified Bessel function, the Coulomb logarithm is about \( \ln L = 20 \), and the dimensionless electron and ion temperatures are

\[
\theta_e = \frac{k_B T_e}{m_e c^2}, \quad \theta_i = \frac{k_B T_i}{m_i c^2}.
\]

The rate simplifies to

\[
F_{ie} = \frac{3}{2} \sqrt{\frac{2 m_e}{\pi}} n^2 d \sigma_T c k_B(T_i - T_e) \left( \frac{m_e c^2}{k_B T_e} \right)^{3/2} \ln L
\]

\[
\approx 1.35 \times 10^{-13} \frac{n^2}{e_{ie}^2} (c^2_e - c^2_i)[\text{erg s}^{-1}\text{cm}^{-3}]
\]

in a non-relativistic case.

The energy equations employ the relativistic electron energy

\[
u_e \approx \frac{3}{2} \frac{0.7 + 2c^2_r n_p/m_e}{0.7 + c^2_r n_p/m_e} m_p c^2 e_{ie},
\]

and the CIE cooling power (Sutherland & Dopita 1993)

\[ P_{cool} = \Lambda(T)n^2 \]

for the cooling rate \( \Lambda(T) \). Then the electron energy balance equation is

\[
\frac{D(\nu_e/m_p)}{Dt} - \frac{c^2_{ie}}{2} \frac{Dn}{Dt} \frac{F_{ie}}{m_p} = -\frac{P_{cool}}{m_p} + f_q g(r)(1 + d)
\]

\[
\times \left( \frac{v^2_{\perp}}{2} + \frac{v^2_m}{2} - \frac{5}{2} c^2_{ie} \right) + \frac{1}{\rho} \partial_r (\rho u_r v_r),
\]

where the effective wind velocity \( v_w \) is given by the formula (4).

The ion energy balance is

\[
\frac{D}{Dt} \left( \frac{3}{2} c^2_{ii} \right) - \frac{c^2_{ii}}{2} \frac{Dn}{Dt} \frac{F_{ie}}{m_p} = f_q g(r)(1 + d)
\]

\[
\times \left( \frac{v^2_{\perp}}{2} + \frac{v^2_m}{2} - \frac{5}{2} c^2_{ii} \right).
\]

While Shcherbakov & Baganafo1 (2010) enhanced the rate of Coulomb collisions to enforce the temperature equality \( T_e = T_i \) in the feeding region, we employ the normal rate of Coulomb collisions.

### 3.3. Free Parameters and Boundary Conditions

We search for the stationary solutions of the system of Equations (9), (11), (19), and (20) with the shooting method. The system has four free parameters: the BH mass \( M_{BH} \), the normalization of the mass source function \( f_q \), the effective supernova wind velocity \( v_w,SN \), and the stagnation point radius \( r_{st} \). Multiple solutions exist, however, for each set of these parameters. We identify a set of the natural boundary conditions and the constraints, which leads to a unique solution. These are

1. equal electron and ion temperatures \( T_i = T_e \) at a large radius,
2. the presence of a sonic point in the accretion flow and the absence of shocks,
3. and the zero gradient of the electron temperature close to the BH \( dT_e/dr = 0 \).

The third condition is practically equivalent to the requirement of the mere existence of the solution down to the BH horizon. We also search for advective solutions of the same system of equations by setting the conductivity to zero. Only the first two conditions are imposed to find a unique advective solution.

### 4. FITTING XVP DATA

Having presented the dynamical model, in this section we discuss the X-ray data and outline the computations of the simulated spectra and the fitting technique. Previous source modeling relied on earlier Chandra observations with 150 ks total exposure (Wong et al. 2011). New observations with a combined exposure 1 Ms were performed in 2012 within Chandra XVP. The new data and their model-independent analysis are presented in a companion paper Wong et al. (2014). The deep X-ray observations of the NGC 3115 nucleus reveal the extended source centered on the BH, which consists of the gas and unresolved point sources.

#### 4.1. CIE or Non-equilibrium Ionization?

The gas temperature is about \( T = 0.3–1 \) keV, so that the emission is dominated by metal lines at \( E \approx 0.8 \) keV (Wong et al. 2011). The line emission power is influenced by the gas ionization state. The collisions of the stellar winds and the shock waves from supernovae lead to the episodes of instantaneous heating. The heating episodes throw the gas into a non-equilibrium ionization (NEI) state. The CIE is restored after a large number of particle collisions. The number of collisions is quantified by the ionization timescale, a product of the density by the time \( \xi = nt \). We estimate \( \xi \) at a 5″ radius, where the density is \( n = 3 \times 10^{-3} \) cm\(^{-3} \) (Wong et al. 2011). The region has a sound crossing time \( t_s \approx 10^6 \) yr, during which about \( N \approx 400 \) supernovae explode. Then the same portion of gas is shocked every \( \Delta t = t_s N^{-1/3} \approx 10^5 \) yr. The ionization timescale between shocks is \( \xi \approx 10^{11} \) s cm\(^{-3} \), for which the flow might not attain full ionization equilibrium (Smith & Hughes 2010). However, as shown below, cooling is relatively weak in the best-fitting flow solutions. A passage of a single shock might not substantially change the gas temperature, so that the effective ionization timescale is much larger, and the CIE assumption is justified. For the gas radiation we use the CIE model apec based on ATOMDB 2.0.1 (Foster et al. 2012) as implemented in XSPEC 12.8 (Arnaud 1996). The NEI effects are to be explored in future work.
4.2. Optical Depth Effects

The optical depth also influences the line emission power. Here we show that the X-ray radiation in the NGC 3115 nucleus is optically thin to both absorption and resonant scattering. Let us make a strong assumption that all the X-ray luminosity is concentrated in a single line. We set the line energy at the peak of the observed gas spectrum $E_{\text{line}} = 0.8$ keV. The temperature in the region is $T \sim 0.4$ keV (Wong et al. 2011), so that the line is subject to thermal broadening by $\Delta v / c \sim 6 \times 10^{-4}$. Let us now compare the blackbody luminosity in this line with the total observed luminosity to estimate the efficiency of absorption. The blackbody source function is

$$B_\nu = \frac{2h\nu^3}{c^2} \exp \left( \frac{h\nu}{k_B T} \right) - 1^{-1}.$$  \hspace{1cm} (21)

Then the blackbody line luminosity is

$$P_{\text{line}} = 4\pi r^2 B_\nu (E_{\text{line}}) \frac{d\nu}{c} \nu_{\text{line}} \sim 10^{39} \text{ erg s}^{-1}$$ \hspace{1cm} (22)

emitted by a sphere with a radius $r = 1''$. This is about 20 orders of magnitude above the observed luminosity.

Resonant scattering may have a larger effect as it is found to change the surface brightness profiles of elliptical galaxies (Shigeyama 1998). Shigeyama (1998) estimate the emission averaged optical depth to be around $\tau_{\text{opt}} \sim 5$ over the scattering column density $N_{\text{sc}} \sim 3 \times 10^{20}\text{cm}^{-2}$ for the relevant gas temperature. The scattering column density to the center of NGC 3115 is about $N_{\text{sc}} \sim 3 \times 10^{18}\text{cm}^{-2}$ and the correspondent optical depth is $\tau_{\text{opt}} \sim 0.05 \ll 1$. Thus, the gas emission is optically thin to both absorption and scattering.

4.3. Point Sources

The contamination by the point sources complicates the modeling of the gas emission. We subtract the brightest isolated objects, but source confusion precludes the reliable subtraction at radii $r \lesssim 4''$. The weaker and confused point sources contribute to the extended emission. A reliable spectral model is the key to discriminate such emission from the gas emission.

LMXBs comprise most of the resolved and some of the unresolved point source emission. The combined spectrum of the resolved LMXBs is an absorbed power-law with index $\Gamma_{\text{LMXB}} = 1.61$ (Wong et al. 2011), and we use the same index to model the unresolved LMXBs. The nuclear LMXB luminosity is proportional to the stellar mass (Gilfanov 2004; Miller et al. 2012). However, as the nuclear luminosity in NGC 3115 is dominated by a few bright sources, the Poisson noise in the proportionality coefficient is large. We leave the normalization of the LMXB luminosity to be a free parameter.

 Cataclysmic variables and coronally active stars contribute to the diffuse X-ray emission as the so-called CV/AB component (Revnivtsev et al. 2006, 2008). Following Wong et al. (2014) we model the CV/AB contribution as an absorbed sum of a power-law with an index $\Gamma_{\text{CV}} = 1.915$ and a thermal component with $T_{\text{CV}} = 0.763$ keV. The total CV/AB luminosity is computed from the $L_K - L_X$ relation and the surface brightness is taken to be proportional to the optical surface brightness. Each CV/AB source is relatively weak, so that many sources contribute to the emission, and Poisson noise is insignificant. The CV/ABs is a sub-dominant component in the inner flow (Wong et al. 2014).

4.4. Point-spread Function

The Chandra observations probe the inner several arcseconds around the supermassive BH in NGC 3115. Since spatial variations are expected on the scale of $\lesssim 1''$, the results of such observations are affected by photon redistribution due to the finite size of the point-spread function (PSF). An implementation of the resultant PSF spreading is generally available in XSPEC as the mixing models, yet no such model exists for the Chandra PSF. We implement the PSF spreading in Mathematica 9 and perform consistency checks. For simplicity, we adopt an energy-independent Gaussian PSF with width $\sigma_{\text{PSF}} = 0'.'27$, which fits the core of the surface brightness profile of a nearby point source.

4.5. Procedure

There are many ways to compare the simulated emission from the accretion flow model to the observations. For example, Shcherbakov & Baganoff (2010) compared the energy-integrated profiles of the surface brightness. This approach introduces a degeneracy between the temperature and the density: the high temperature low density model produces the same surface brightness as the low temperature high density model. The degeneracy may be broken with the use of the spectrum. Fitting the radius-integrated spectrum (Wang et al. 2013) one obtains the relative contributions of gas at the different temperatures with little information about the spatial distribution. Thus, we maintain both the spectral and the spatial information, while comparing the simulated emission to the data.

Following Wong et al. (2014) we divide the BH feeding region into circular rings centered on the BH. In this paper we limit ourselves to an outer radius of $12''$, which is far outside of $r_B$. We define seven rings with the projected radii in the ranges $0''-1''$, $1''-2''$, $2''-3''$, $3''-4''$, $4''-5''$, $5''-8''$, and $8''-12''$. The spectrum of each ring is extracted and grouped with a minimum of 25 photons per bin for a total of 247 bins over the 7 rings. Having defined the observed spectra, we calculate the simulated spectra and compute the chi-square statistic.

The simulated spectrum in each ring is the sum of the fixed CV/AB contribution, the fixed background, the power-law LMXB component with a free normalization, and the gas component. Since the background dominates at high energies, we set the high energy limit at $E_{\text{max}} = 6$ keV. We set the low energy limit at $E_{\text{min}} = 0.5$ keV as the lowest bin energy for the grouped observed spectrum.

The gas properties are defined by the computed profiles of the temperatures $T(r)$ and $T_e(r)$ and the electron density $n(r)$ for the radius from $r_{\text{min}} = 2000r_g = 4 \times 10^{-3}$ arcsec to $r_{\text{max}} = 7.8 \times 10^9 r_g = 16''$. We set the density to zero outside of this radial range. We calculate the simulated spectra fully self-consistently. We divide the flow into many spherical shells and compute the contributions of each shell into the projected rings, while taking into account the PSF spreading. We find a joint $\chi^2$ as a sum over all seven rings. We perform the steepest descent search for a minimum of $\chi^2$ over the set of the model parameters. We explore the BH masses in the range $M_{\text{BH}} = (0.7-2.0) \times 10^9 M_\odot$ motivated by the dynamical modeling of the stellar motions (Kormendy et al. 1996; Emsellem et al. 1999). We do not restrict the other three free parameters $f_g$, $v_{\text{w,SN}}$, and $r_{st}$. We find the best-fitting conductive and advective solutions.
5. RADIAL INFLOW–OUTFLOW SOLUTIONS

5.1. Solutions with Conduction

The dynamical structure of the best-fitting solution with conduction is shown in Figure 4. This solution is achieved at the lower BH mass boundary \( M_{\text{BH}} = 0.7 \times 10^9 M_\odot \) for the mass loss rate normalization \( \dot{M}_\text{f} = 0.150 \), the effective supernova wind velocity \( v_{\text{w,SN}} = 521.6 \, \text{km} \, \text{s}^{-1} \), and the stagnation point radius \( r_* = 0.33 \). It reaches \( \chi^2/\text{dof} = 1.001 \) for \( \text{dof} = 236 \) and has an accretion rate \( \dot{M} \approx 2 \times 10^{-3} M_\odot \, \text{yr}^{-1} \). This accretion rate is a factor of 100 lower than Bondi accretion rate (Wong et al. 2011). However, the correspondent accretion power \( \dot{M} c^2 \approx 10^{43} \, \text{erg} \, \text{s}^{-1} \) is still about 7.5 orders of magnitude larger than the observed jet radio power. The density (shown in the top panel) behaves approximately as \( n \propto r^{-1} \) over the large range of the radius. The density does not flatten out outside of the Bondi radius. The electron temperature is higher than the ion temperature due to heat conduction, which primarily influences the electrons. The ion temperature is approximately virial at all radii, which corresponds to \( T_i \propto r^{-1} \) in the inner flow. The slope of \( T_i \) is relatively flat in the outer flow, where the enclosed mass increases with radius as \( M_{\text{enc}} \propto r \), so that \( T_i \propto M_{\text{enc}} r^{-1} \propto r^0 \). The gas inflow velocity (shown in the bottom panel) exceeds the sound speed at a relatively large radius \( r \sim 10^3 r_g \). This is a consequence of the rising electron heat capacity (Shcherbakov 2008) and the absence of super-virial heating. The outflow velocity is much below the sound speed in the outer flow, so that the outflow is subsonic. The determined stagnation point radius corresponds to the circularization radius of \( r_{\text{circ}} = 2500 r_g = 5 \times 10^{-3} \, \text{arcsec} \) according to Figure 3. Relatively little X-ray emission originates within this radius in a non-cooling accretion flow.

In the middle panel of Figure 4 we depict the 90% confidence range of the temperature (green/light area) in the “single-T apec per annulus” best-fitting model presented in Wong et al. (2014). In this model the observed spectrum in each annulus is fitted independently with a single-temperature apec component instead of drawing the gas temperatures from a smooth radial profile. The point source and the background contributions are computed the same way in both kinds of models. The temperature in the “single-T apec per annulus” best-fitting model agrees with the temperature in the best-fitting conductive solution at large radii \( r > 2'' \), but deviates down in the inner flow.

As we show in Figure 5 the “single-T apec per annulus” model reaches lower \( \chi^2/\text{dof} = 0.895 \) with the more uniform residuals \( \Delta(\chi) \). The best-fitting solution with conduction underpredicts the observed soft flux as evident from the systematic trend at the lowest energies in the top panel. In sum, while our solution could be improved with the lower temperature in the inner flow, it already provides an acceptable fit to the data with \( \chi^2/\text{dof} = 1.001 \). The reasons for this underprediction are explored in Wong et al. (2014), the main hypothesis being the presence of an inner soft component, which appears to be extended. This soft component could either be a cool diffuse gas or a distinct population of point sources. Wong et al. (2014) develop a two-component gas model and obtain a temperature profile of the hotter component, which agrees with the best-fitting profile of the electron temperature. The data and the model are shown for selected annuli in Figure 6 for low BH mass \( (0.7 \times 10^9 M_\odot) \) and high BH mass \( (1.8 \times 10^9 M_\odot) \) best-fitting solutions with conduction. Lack of strong soft emission is evident in both the inner and the outer annuli for both BH masses. Substantial non-thermal emission convolved with Chandra response function is responsible for 1.9 keV bump in the outer annuli, while the extended bump in 1.3–1.9 keV energy range in the inner annuli is mainly emitted by the hot inner accretion flow. The annuli with projected radii within 3–4'' exhibit relatively soft spectrum, while the models are substantially harder. As indicated by “single-T apec per annulus” model, a hotter thermal plasma provides a better fit to that spectrum. Since the galactic gravitational potential dominates the BH potential at \( \gtrsim 1'' \) distance, then the differences between the low BH mass and the high BH mass models are the...
most evident in the inner annulus. The high BH mass model has a higher virial temperature. This leads to further underprediction of the soft flux emitted by the inner accretion flow, so that high BH mass model provides a worse fit to the data.

5.2. Advective Solutions and Comparison

We explore not only the solutions with conduction, but also the advective solutions, where the conductivity is set to zero. The comparison between these cases helps to explore the role of conduction. In Figure 7 we show the dynamical quantities for the best-fitting solution without conduction (dashed) and for the best-fitting solution with conduction (solid). The best fit among the advective solutions is also achieved at the lower BH mass boundary $M_{\text{BH}} = 0.7 \times 10^9 M_\odot$. The correspondent values of the free parameters are $f_q = 0.289$, $v_{w,\text{SN}} = 510.0 \text{ km s}^{-1}$, and $r_{\text{st}} = 1.08$. This solution reaches $\chi^2/\text{dof} = 0.998$ and has an accretion rate $\dot{M} \approx 2 \times 10^{-3} M_\odot \text{ yr}^{-1}$. The values of the free parameters are similar in the best-fitting conductive and advective solutions, except the stagnation point is much further out in the advective solution and the accretion rate is much higher. This difference is a natural consequence of conduction. The density profiles in both best-fitting solutions asymptote to the steep Bondi profile $n \propto r^{-3/2}$ in the inner flow. However, the inner flow density and the accretion rate are a factor of ten higher in the advective solution. This factor may be even larger, when super-virial heating is included (Johnson & Quataert 2007; Shcherbakov & Baganoff 2010). As super-virial heating is likely important in the inner flow, the computed accretion rate is an upper limit on the rate of mass crossing the event horizon. The electron temperature in the advective solution is lower than the ion temperature $T_e < T_i$ due to cooling in the outer flow and the higher electron heat capacity in the inner flow. The solution with conduction has a factor of three lower inner ion temperature. The energetics of the outer flow are mainly determined by the mass injection and the energy injection, so that the properties of the outer flow are similar between the two best-fitting solutions.

One of the most important results of the presented model fitting is the BH mass. In Figure 8 we show the reduced $\chi^2$ as a function of the BH mass for both the best-fitting advective models (red/dashed line) and the best-fitting models with conduction (blue/solid line). Both types of models show
Figure 7. Comparison of the dynamical quantities in the best-fitting solutions with and without conduction: density (top panel), temperature (middle panel), and radial velocity (bottom panel). We show the quantities in the conductive solution (thick solid lines), the quantities in the advective solution (thick dashed lines), and the simple power-laws (thin lines). Shown in the middle panel are the electron temperature $T_e$ (blue/upper solid line) and the ion temperature $T_i$ (red/lower solid line) for the solution with conduction, the electron temperature $T_e$ (blue/upper dashed line) and the ion temperature (red/lower dashed line) $T_i$ for the advective solution. Note that $T_e > T_i$ in the conductive solution, while $T_e < T_i$ in the advective solution. The density is shallower in the flow with conduction. Both density profiles asymptote to $n \propto r^{-3/2}$ and both ion temperature profiles asymptote to $T_i \propto r^{-1}$ in the inner flow. The conductive solution has the sonic point closer in, while the inner asymptotic velocities are comparable in two models.

(A color version of this figure is available in the online journal.)

a clear rising trend with the BH mass in agreement with Figure 6 and discussion of the spectral features therein. The 90% confidence range limits the BH mass to below $1.1 \times 10^9 M_\odot$ for the conductive models and to below $1.3 \times 10^9 M_\odot$ for the advective models in agreement with the latest BH mass estimates (Emsellem et al. 1999). However, the adopted modeling has many caveats, which should be carefully examined before the firm conclusions are drawn about the BH mass. Here we demonstrate that it is possible to discriminate between the models with the different BH masses by fitting the X-ray data. We discuss the caveats of the modeling in the next section.

6. DISCUSSION AND CONCLUSIONS

6.1. Summary of Results

In the paper we present the modeling of the X-ray data from 1 Ms $Chandra$ XVP observation of the NGC 3115 center. We connect the properties of the nuclear star cluster known from optical observations to the properties of the X-ray emitting hot gas. We construct the radial inflow–outflow dynamical models, which include many physical effects: the matter and the energy injection by stellar winds and supernovae, conduction, the additional gravitational pull by the enclosed mass, cooling, and Coulomb collisions. We simulate the X-ray emission from the models and fit the set of the X-ray spectra in concentric annuli around the BH. We find best-fitting models with an acceptable $\chi^2$/dof $\approx 1.00$. The proposed models are sensitive to the BH mass and favor low values $< 1.3 \times 10^9 M_\odot$. We estimate the normalization of the mass source function to be $f_q \approx 0.15 - 0.30$, which is somewhat smaller than the expected value $f_q = 1$. We discuss below the reasons for the deviation of $f_q$ from unity distinct from the uncertainties in the mass loss rate. The best-fitting effective supernova wind velocity is $v_{w,SN} \approx 521 \text{ km s}^{-1}$, which corresponds to the rate of the supernova explosions $R_{SN} \sim 3 \times 10^{-14} M_\odot \text{ yr}^{-1}$ for the fiducial energy release $E_K = 10^{51} \text{ erg s}^{-1}$ per event. This estimated event rate is consistent with the observed event rate in S0 galaxies like NGC 3115 (Mannucci et al. 2005). The stagnation point is at $r_{st} \approx 0\prime.33$ for the best-fitting solution with conduction and at $r_{st} \approx 1\prime.08$ for the best-fitting advective solution. Therefore most of the “accretion flow” seen by $Chandra$ is outflowing from the region, while the stagnation radius scale is barely resolved. We find that the best-fitting conductive and advective solutions behave similarly in the outer flow, yet the advective solution has the higher density and the lower electron temperature in the inner flow.
It is instructive to compare the relative strengths of the various effects by computing the correspondent timescales. In Figure 9 we plot the timescales in the feeding region. The sound crossing time (blue/upper thick solid line)

\[ t_s = \sqrt{\frac{3}{5}} \frac{r}{c_{se}} \]  

(23)

is about the free-fall time (green/lower thick solid line)

\[ t_{ff} = \frac{r}{c} \left( \frac{1}{r_g} + \frac{M_{\text{enc}}}{M_B} \right)^{-1} \]  

(24)

so that the gas temperature is close to virial at any radius. We also plot the cooling time (brown/short-dashed line)

\[ t_{\text{cool}} = \frac{n}{F_{\text{cool}}} \]  

(25)

the conductive heating time (magenta/long-dashed line)

\[ t_{\text{cond}} = \frac{n}{Q_+} \]  

(26)

where \( Q_+ = -\text{div}(F_{\text{cond}}) \)

is the divergence of the conduction heat flux, and the mass injection time (red/dot-dashed line)

\[ t_{\text{inj}} = \frac{n}{f_q q} \]  

(27)

The cooling timescale is about 100 times the free-fall timescale \( t_{\text{cool}}/t_{\text{ff}} \sim 100 \), so that cooling is expected to be unimportant in the modeled hot-phase gas in the non-rotating flow (Gaspari et al. 2013). The mass injection time is much larger than either \( t_s \) or \( t_{\text{ff}} \), which indicates a relatively slow radial gas velocity \( v_r \sim 0.1 c_s \). The conductive heating time is very large outside of \( r \sim 1'' \), so that the solutions with and without conduction behave similarly in the outer flow. This timescale gets comparable to the injection time inside of \( r \sim 1'' \), which suggests the importance of conduction at those radial scales. The comparison of timescales also helps to establish the self-consistency of the model. The time between consecutive supernova explosions (black/thin solid line)

\[ t_{\text{SN}} = \frac{2E_K}{4\pi r^3 f_q q m_p v_{SN}^2} \]  

(28)

becomes longer than the sound crossing time at \( r \sim 1'' \). Thus, the energy injection from the supernovae cannot be treated on average in the inner flow. However, this mechanism is subdominant at \( r \lesssim 1'' \) as evident from the middle panel in Figure 2: the collisions of stellar winds supply most of the energy in the inner flow. The inner accretion flow experiences relatively weak disturbances from supernova explosions, which are washed away on the dynamical timescale. Then the average energy injection rate is well-defined at any radius.

6.2. What Does the Density Slope Mean?

The modeling of the resolved X-ray emission gives the gas density slope. We find the shallow density profile \( n \propto r^{-\beta} \) with \( \beta \approx 1 \) across a large range of scales in the NGC 3115 nucleus. As briefly discussed in Section 3.1, the shallow density profile commonly occurs in CDAFs (Quataert & Gruzinov 2000; Narayan et al. 2000), in the accretion flows with conduction (Johnson & Quataert 2007; Shcherbakov & Baganoff 2010), and in the accretion flows with the outflows above and below the midplane (Blandford & Begelman 1999; Yuan et al. 2003, 2012b). However, there are other reasons to have \( \beta \approx 1 \) near the Bondi radius in the hot gas flows. Let us elaborate on the effects either directly responsible for the shallow density profile or calling for the extension of the aforementioned explanations.

First, we examine the original Bondi solution as computed by Bondi (1952). Their curve II in Figure 5 shows the relevant case of an adiabatic transonic inflow for the adiabatic index \( \Gamma = 5/3 \). In this solution the density slope \( \beta \) is a function of radius and changes from \( \beta = 0 \) at \( r \gg r_B \) to \( \beta = 1.5 \) at \( r \ll r_B \). The steep asymptotic behavior \( n \propto r^{-3/2} \) is achieved only very deep inside the Bondi sphere. The Bondi flow has \( \beta = 1.0 \) at a tenth of the Bondi radius \( r = 0.1r_B \), which corresponds to their dimensionless radius \( x = 0.2 \). The slope at a radius \( r = 0.5 \) probed by the Chandra satellite in NGC 3115 is expected to be \( \beta < 1 \) even in a fully advection-dominated Bondi-like flow.

Second, we model the material in NGC 3115 to outflow from the stagnation point at \( r_{st} \lesssim 1'' \). However, when the mean radial velocity is much smaller than the sound speed \( v_r \ll c_s \), then the small-scale feedback and the outflows have the same power for both positive and negative \( v_r \). The pressure balance is practically hydrostatic for small \( v_r \) and is given by the Equation (7). Then small-scale feedback and outflows make the density profile shallow in both the inflow region and the outflow region. However, the density in the outflow asymptotes to \( n \propto r^{-2} \), if the radial velocity is large, while the density is constant \( n = \text{const} \) in the Bondi inflow. Models with large outflow velocity \( v_r \sim c_s \) are disfavored for NGC 3115, while being viable for Sgr A* (Quataert 2004).

Third, continuous mass injection modifies the mass conservation law, so that \( M \propto n v_r r^2 \neq \text{const} \). Mass injection is the dominant term in the density balance at radii 0.5–10'' in the best-fitting solution with conduction. Then mass conservation law is inapplicable in the feeding region of NGC 3115 near the Bondi radius \( r \sim r_B \). The density slope in the outer flow is influenced by the matter source term.
Fourth, the region near and outside of the Bondi radius \( r \gtrsim r_B \) is influenced by the gravity of the enclosed mass. The correspondent gravitational potential does not flatten, but increases with radius. Then the gas outflow velocity stays small and the asymptotic outflow behavior is not reached. The virial temperature is much higher in the outer gas, when the enclosed mass from the nuclear star cluster is included. As the gas temperature closely follows the virial temperature, the change in the virial temperature profile influences the density profile. The density profile \( n \propto r^{-1} \) is commonly observed in the hot flows outside of the Bondi radius (Allen et al. 2006; Wong et al. 2011), where the galactic gravitational potential matters. The interplay of these four processes and effects determines the gas density profiles in the LLAGNs. Despite the slope \( n \propto r^{-1} \) approximates the density profile in NGC 3115 over a large radial range, the local slope \(-d \log n/d \log r\) at a given \( r \) often substantially deviates from \( \beta = 1 \). The absence of a single behavior over a large dynamic range demotivates us from isolating the self-similar solutions.

6.3. Limitations of the Dynamical Model

Despite being able to fit the data, the presented models are not fully self-consistent. Let us examine the drawbacks and the limitations of the models and outline a more self-consistent treatment.

6.3.1. Inhomogeneous Medium

The observational studies of Sgr A* suggest inhomogeneous gas near the Bondi radius (Baganoff et al. 2003; Munro et al. 2008; Wang et al. 2013). Regions with vastly different temperatures readily co-exist, while the Chandra satellite only sees the hot dense counterparts with temperature \( T > 0.3 \) keV. Nevertheless, the observed gas temperature \( T = 0.3–1 \) keV in NGC 3115 agrees well with the virial temperature \( T \sim T_v \), and the observed density is reproduced with the normalization of the mass source function \( f_q \) on the order unity. Then the hot gas likely constitutes the dominant gas component.

The filling factor of this hot component may still be below unity \( f_V < 1 \). In this case the mean density required to reproduce the observations is lower. More generally, gas with lower mean density reproduces the observations, when substantial density fluctuations are present. Since the emissivity is proportional to \( n^2 \), then thinking of the best-fitting density as the root-mean-squared quantity effectively takes the inhomogeneities into account.

6.3.2. Non-stationary Solutions

A wide range of non-stationary behaviors, such as oscillation cycles, may occur in accretion flows. The best-fitting energy of the outflowing gas is barely enough to escape the gravitational potential of the enclosed mass. The temperatures in the best-fitting “single-T apec per annulus” model are even lower (Wong et al. 2014), so that the gas may be unable to escape. When the gas inflow rate is limited and the outflow rate is zero, matter gradually accumulates in the BH feeding region owing to stellar mass loss.

The accumulation of matter leads to a higher density, and the gas eventually cools. Cooling leads to a higher accretion rate, since the cooler gas does not counteract the gravity and since accretion is not inhibited by small-scale feedback, when the temperature is sub-virial. The burst of accretion empties the feeding region. The accretion rate drops after the burst, and then a new phase of matter accumulation begins. The accumulation phase of such accumulation–accretion cycles might reproduce the current state of NGC 3115. This possibility is to be explored with future time-dependent numerical simulations.

6.3.3. Angular Momentum Transport

We did not explicitly treat angular momentum transport, which is partially justified a posteriori. We find a relatively small circularization radius \( r_{ec} \lesssim 0.05 \) in the best-fitting solutions. The accretion flow at \( r = 0.5–10^9 \) probed with Chandra might not feel the difference with an explicit treatment of the inner flow circularization. The sonic point in the circularized flow is closer to the BH (Popham & Gammie 1998), and the influence of conduction is expected to be stronger. Then the shallow density profile is expected to continue down to several \( r_g \). Having defined the injection of the angular momentum, we leave angular momentum transport and the inner flow connection for future work.

6.4. Limitations of the Radial Solutions

The presented modeling is performed under the strong approximation of one dimension. The resultant treatment of gravitational forces is approximate and gas motions are restricted.

We compute the enclosed mass profile based on the surface brightness along the semi-major axis assuming zero ellipticity \( \varepsilon = 0 \) of the stellar distribution. However, Kormendy & Richstone (1992) report an ellipticity of \( \varepsilon \approx 0.4 \) at the Bondi radius. Since the ellipticity varies with radius and the gravitational force is not trivially determined for a non-spherical mass distribution, we do not improve in this work upon the zero ellipticity approximation.

The gravitational force is generally lower in the case of non-zero ellipticity. To test the effect of a lower gravitational force we search for a best-fitting solution with a smaller enclosed mass \( M_{enc,x} = 0.7 M_{enc} \) and a fixed BH mass \( 1 \times 10^9 M_\odot \). We find the best-fitting advective solution with a higher normalization \( f_q = 0.59 \) of the mass source function compared to \( f_q = 0.28 \) for the 100% of the enclosed mass. The resultant normalization \( f_q \) is much closer to unity, while \( f_V \) varies little across the best-fitting solutions with different \( M_{BH} \). The effective supernova wind velocity is \( v_{w,SN} = 498 \) km s\(^{-1}\) for the 70% of the enclosed mass compared to \( v_{w,SN} = 455 \) km s\(^{-1}\) for the 100%. The correspondent change of the stagnation radius is from \( r_{st} = 1'52 \) to \( r_{st} = 1'12 \). The reduced chi-squared shows a small improvement by \( \Delta(x^2/\text{dof}) = 4 \times 10^{-3} \).

The gas in the one-dimensional solution is restricted to either inflow or outflow radially. More complex patterns may occur in two dimensions, such as inflow in the equatorial plane with outflow along the angular momentum axis. While typical density and temperature profiles in two-dimensional solutions may be similar to those in one-dimensional solutions (Yuan et al. 2012b; Sadowski et al. 2013), more detailed fitting of the data with the two-dimensional solutions is warranted. The lower gravitational force facilitates the outflow along the angular momentum axis. This leads to an easier evacuation of the feeding region, so that the best-fitting two-dimensional solutions are expected to have a higher normalization \( f_q \) of the mass loss rate. Finding the self-consistent two-dimensional solutions might require the numerical simulations, and the present manuscript provides a starting point for such work.

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