Comprehensive entropy weight observability-controllability risk analysis and its application to water resource decision-making

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Abstract

Decision making for water resource planning is often related to social, economic and environmental factors. There are various methods for making decisions about water resource planning alternatives and measures with various shortcomings. A comprehensive entropy weight observability-controllability risk analysis approach is presented in this study. Computing methods for entropy weight (EW) and subjective weight (SW) are put forward based on information entropy theory and experimental psychology principles, respectively. Comprehensive weight (CW) consisting of EW and SW is determined. The values of observability-controllability risk \( R_c \) and gain by comparison \( G_c \) are obtained based on the CWs. A case study on selection of water resource planning alternatives and measures in the Yellow River Basin, China, was performed. Results demonstrate that the approach presented in this study can achieve optimal decision-making results.

Keywords: decision making, entropy weight risk analysis, observability-controllability risk, gain by comparison, Yellow River Basin

Introduction

Water resource planning is a complex, multifactorial and multi-objective decision process involving the participation of multiple stakeholders (Wang et al., 2002) and possessing the characteristics of multidisciplinary complexity, domain-dependent knowledge, institutional constraints and cultural dimensions (Cai et al., 2004). It could result in uncertain consequences, complex interactions, and participation of multiple stakeholders with conflicting interests (Hyde et al., 2004). Decision makers are asked to select the best alternative. This decision process is always accompanied by risk. The uncertainty and risk are inevitable in planning and operation of water resource engineering, which may lead to failure in achieving the expected goals. Reliability is the capability to satisfy the requirements of the system while risk is the cost of being unreliable (Kenward et al., 1999). It is necessary to develop effective models and methods for selection of the best alternative, so as to provide strategic support for decision makers, reduce the time for problem solving and increase the probability of a better solution (Cai et al., 2004).

Over the years, many quantitative methods have been developed to facilitate making rational decisions involving multiple criteria (Islam and Abdullah, 2006), such as the analytic hierarchy process (Saaty, 1980), multiple objective analysis (Haines and Hall, 1974; Cohon, 1978; Raju et al., 2000; Hyde et al., 2004), open and shared vision modelling (Palmer, 1999; Loucks, 2000), decision support system (Westphal et al., 2003) or group decision support system (Cai et al., 2004), uncertainty-based sensitivity analysis method (Barron and Schmidt, 1988; Triantaphyllou and Sanchez, 1997) and risk analysis (Haines, 1998; Ezell et al., 2000). These methods or their combinations are to a certain extent effective solutions to the problems, but they have some inherent shortcomings. For example, for the multiple objective analysis method, an important issue is to represent competing objectives clearly and unambiguously to decision makers (Cai et al., 2004), but it is often difficult to provide satisfying objectives for all decision makers and errors may arise to a certain extent when the method is simplified excessively by reducing multiple objectives to one or two. In open and shared vision modelling, planning objectives and performance measures are often incorporated into a single framework to allow for the generation and evaluation of alternatives and to facilitate conflict resolution (Palmer, 1999); however, the incorporation is uncertain and not perfect or feasible. In addition, due to the subjective restriction and diversification of experts coming from different domain-dependent knowledge backgrounds and levels, there are some inevitable insufficiencies and limitations for the decision support system and group decision support system methods. The uncertainty-based sensitivity analysis and risk analysis methods can be used to analyse the change relationships between the input data and the outcomes, but they are incapable of solving their inherent uncertainties and risks (Hyde et al., 2004). The analytic hierarchy process (AHP) is regarded as one of the most successful techniques to solve decision-making problems involving multiple criteria. In AHP, a number of pair-wise comparison matrices are formed in order to derive weights of the criteria and the local weights of the alternatives. The alternative with the highest global weight is selected as the best one (Islam and Abdullah, 2006). But the AHP has some inherent drawbacks: It requires a large number of pair-wise comparisons, especially in the presence of a large number of criteria, and the exhaustive pair-wise comparison is
tedious and time consuming when there are many alternatives to be considered (Hotman, 2005; Islam and Abdullah, 2006; Liebowitz, 2005).

The aim of this study is to present a simple analysis approach called comprehensive entropy weight observability-controllability risk analysis (CEWORA), based on information entropy theory (IET) and experimental psychology principles (EPP). A case study of water resource planning in the Yellow River Basin, China, was performed. In the rest of this paper, we first introduce the general concept of IET, then present the method of CEWORA and apply it to the decision of alternatives and measures in the case study.

Methods

General concept of information entropy

The concept of entropy originates from thermodynamics and represents the heat energy that cannot be used to generate work. It is a ratio of the heat of temperature. In 1948, Shannon and Weaver (1948) introduced the entropy concept into information theory and measured the amount of information with it. Information entropy is a ratio of the variation of heat to the variation of temperature. In 1948, Shannon and Weaver (1948) introduced the entropy concept into information theory and measured the amount of information with it. Information entropy is a

\[ H(x) = -\sum_{x} f(x) \cdot \log(f(x)) \]

where:

- \( f(x) \) is probability density function of independent variable \( x \).

The unit of information entropy varies with the logarithms' base: the unit of base 2 is bits, base 10 is decibels and base natural-logarithm is napiers (Amorochi and Espildora, 1973). The base 2 logarithm is considered in this study.

According to Eq. (1), the probability density function \( f(x) \) needs to be continuous. However, measurements are usually discrete, representing data sets that are limited in time and space in the case of laboratory or field data (Mays et al., 2002). Under this condition, suppose that a system has \( n \) kinds of states; the discrete equation is given by:

\[ H(x) = -\sum_{x} p_i \cdot \log(p_i) \]

where:

- \( p_i \) is the probability of the \( i \)th state, subject to the condition \( \sum_{i=1}^{n} p_i = 1 \)

Comprehensive entropy weight observability-controllability risk analysis

The approach is carried out based on the following steps:

- **Step 1:** Suppose that there are \( m \) decision-making alternatives. Each alternative includes \( l \) indexes. The \( i \)th alternative with the \( j \)th index has a value of \( k_{ij} \). A decision-making matrix of \( Q = (k_{ij})_{m \times l} \) is constructed.

- **Step 2:** Standardise the matrix \( Q \) and mark it standardisation matrix \( D, D = (d_{ij})_{m \times l} \), where \( d_{ij} \) is calculated as follows:

\[ d_{ij} = k_{ij} / \max(k_{1j}, k_{2j}, \ldots, k_{mj}) \]

- **Step 3:** Normalise the matrix \( D \) and mark it normalisation matrix \( P, P = (p_{ij})_{m \times l} \), where

\[ p_{ij} = d_{ij} / \sum_{i=1}^{m} d_{ij}, \text{meets} \sum_{i=1}^{m} p_{ij} = 1, i=1,2,\ldots , m \text{and} j=1,2,\ldots , l. \]

According to Eq. (2), the information entropy of the \( j \)th evaluation index is

\[ E_j = -\sum_{i=1}^{m} p_{ij} \cdot \log_2(p_{ij}) \]

- **Step 4:** When \( p_{i\cdot j} = p_{j\cdot} = \sum_{i=1}^{m} p_{ij} / m \), there exists the maximum entropy \( E_{\max} = \log_2 m \). Then the evaluation entropy value of the \( j \)th index is defined as:

\[ e_j = -E_j / E_{\max} \]

The evaluation entropy indicates the important degree of index. The smaller the value of \( e_j \), the greater the information content provided by the \( j \)th index (Ding and Shi, 2005).

- **Step 5:** On the basis of Eq. (5), the entropy weight (EW) of the \( j \)th index in the comprehensive appraisal is defined as follows:

\[ \theta_j = \frac{1 - e_j}{l - \sum_{j=1}^{l} e_j} \]

where:

- \( \theta_j \) is the entropy weight of the \( j \)th index and
- \( 0 \leq \theta_j \leq 1 \), \( \sum_{j=1}^{l} \theta_j = 1 \)

The EW calculated by Eq. (6) is an objective weight, which depends on the inherent information of decision alternatives.

- **Step 6:** The experience and judgment from decision makers cannot be ignored in the decision-making process, a subjective weight (SW) of index is presented as follows, based on the EPP:

\[ \delta_j = F(j) / \sum_{i=1}^{l} F(i) \]

where:

- \( F(i) \) is the degree of membership of the \( i \)th index

\[ F(i) = \frac{\log(l+2)}{\log(l+1)}, i=1,2,\ldots, l \]

It is the degree of membership of the \( i \)th index.

- **Step 7:** Combining the EW with the SW, the comprehensive weight (CW) is defined as:

\[ w_j = \frac{\delta_j \theta_j}{\sum_{j=1}^{l} \delta_j \theta_j} \]

where:

- \( w_j \) is the CW of the \( j \)th index and \( 0 \leq w_j \leq 1 \).

The comprehensive weight matrix \( W \) can be built based on all the combined situations of 5 CWs of \( w_j \) for \( n = (l-1) \cdot (l-2) \cdot 2 \cdot 1 \).

- **Step 8:** A type of risk called observability-controllability

\[ d_{ij} = k_{ij} / \max(k_{i1}, k_{i2}, \ldots, k_{in}) \]

\[ \sum_{i=1}^{m} p_{ij} = 1, i=1,2,\ldots , m \text{and} j=1,2,\ldots , l. \]

\[ E_j = -\sum_{i=1}^{m} p_{ij} \cdot \log_2(p_{ij}) \]

\[ e_j = -E_j / E_{\max} \]

\[ \theta_j = \frac{1 - e_j}{l - \sum_{j=1}^{l} e_j} \]

\[ \delta_j = F(j) / \sum_{i=1}^{l} F(i) \]

\[ w_j = \frac{\delta_j \theta_j}{\sum_{j=1}^{l} \delta_j \theta_j} \]

\[ 0 \leq w_j \leq 1. \]

\[ n = (l-1) \cdot (l-2) \cdot 2 \cdot 1. \]
risk ($R_w$) is proposed to indicate the risk that the expected targets cannot be achieved. It results from the uncertainty of the observability-controllability objectives and results, and the limitation of capacity of executants. According to the observability-controllability model of periphery (COMP) presented by Li and Wei (2011), a certain relationship exists between the system inner state and the system input and output. In terms of the feedback information from the system, the controller could make corresponding responses and take some measures to control the system inputs, outputs and states, based on the changing relationship between the system and the environment, in order to promote the coordinated and stable development of the system. This process continues until the termination condition or the system objective required is fulfilled. The key factor leading to the problems mentioned above is the disharmony between the surface water–soil–environment system, such as water resource shortages, flooding, and deterioration of ecological function.

The flow chart of the approach is shown in Fig. 1.

According to Eq. (10), a close relationship exists between $G_w$ and $R_w$. The greater the $G_w$ is, the greater the $R_w$ is. It indicates that huge risk could be changed into huge gain. Under the permitted value range of risk, the alternative with the largest risk value has the greatest benefit in general. If the real allowable value of risk is set as a certain value, such as $R_w$, then only the alternative with the greatest gain and satisfying the condition of $R_w \leq R_0$ could be adopted as the optimal one. Therefore, optimal decision results can be achieved based on the alternative with the greatest value of $R_w$ or $G_w$ under the permitted condition of risk.

**Case study**

**Statement of the problem**

The Yellow River (YR) originates on the Qinghai-Tibet Plateau, China, and makes its way to the Bohai Sea (Fig. 2). The river is the second-longest (5 464 km) in China and its basin covers an area of 722 000 km$^2$. The total average yield is about 72.8 x 10$^3$ m$^3$.

With the development of economy and society, the water requirements in the Yellow River Basin (YRB) have increased rapidly. The Yellow River has one of the highest water resource exploitation intensities in the world. For example, the total amount of water consumption by industry, agriculture and domestic uses was 42.1 x 10$^3$ m$^3$ in 1998, accounting for 72.5% of the average annual runoff (AAR), and 48 x 10$^3$ m$^3$ in 2000, 82% of the AAR (RPDRI, 2001). The intensity of demand for water resources and the alteration of natural conditions have resulted in the occurrence of water resource problems in the YRB, such as water resource shortages, flooding, and deterioration of ecological function.

The key factor leading to the problems mentioned above is the disharmony between the surface water–soil–environment system and the environment, in order to promote the coordinated and stable development of the system. This process continues until the termination condition or the system objective required is fulfilled.

The gain by comparison ($G_{ic}$) is the subsystems’ relative income share per unit payout or investment when both the total investment and income of the system approach 100% under the risk condition, which is shown as:

$$G_{ic} = \left(1 - \frac{r_{ic}}{v_{ic}}\right)$$  \hspace{1cm} (10)

The flow chart of the approach is shown in Fig. 1.

According to Eq. (10), a close relationship exists between $G_{ic}$ and $R_{oc}$. The greater the $G_{ic}$ is, the greater the $R_{oc}$ is. It indicates that huge risk could be changed into huge gain. Under the permitted value range of risk, the alternative with the largest risk value has the greatest benefit in general. If the real allowable value of risk is set as a certain value, such as $R_{oc}$, then only the alternative with the greatest gain and satisfying the condition of $R_{oc} \leq R_0$ could be adopted as the optimal one. Therefore, optimal decision results can be achieved based on the alternative with the greatest value of $R_{oc}$ or $G_{ic}$ under the permitted condition of risk.

**Figure 1** Flow chart indicating the process for comprehensive entropy weight observability-controllability risk analysis

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system and the social-economic system in YRB. The exploitation and utilisation of water resources should be consistent with the natural laws of water resources. However, intensive human activities have strongly altered the natural water cycle, leading to serious contradictions between supply of and demand for water resources. In order to achieve the sustainable development of water resources, it is necessary to use water saving, water recycling, water transfer and flood utilisation processes in the YRB.

Alternative measures to solve water resource problems in the Yellow River Basin

In order to achieve harmonisation between demand and supply of water resources, attention should be given to balancing the demand and supply sides of water resource management. The supply side here indicates the quantity of water resource supply, including surface and groundwater, in terms of current exploitation and utilisation capability; while the demand side mainly denotes the quantity of demand for water resources forecast by future planning. The difference and contradiction between the two sides should be considered.

With regard to this situation, some feasible ways to solve the water resource problems in YRB have been suggested, after the appropriate consultation, appraisal and assessment of Chinese governors from the Yellow River Conservancy Commission, stakeholders from all walks of life, experts from all backgrounds and researchers and academics from universities. The suggested methods include: water saving in industry (WSI) and agriculture (WSA); water transfer from the South-to-North Water Transfer Project (WTP) of China (see Fig. 2); recycling utilisation of sewage (RUS); and floodwater utilisation (FWU).

The WSI and the WSA are implemented to cut down the water demand and both are considered to yield a water-saving rate of 10%. The WTP is executed so as to increase the available water supply of YRB. Water is proposed to be transferred from the Yangtze River Basin to the YRB to supplement the water supply. A water volume of 2 or 3 x 10^9 m^3 transferred from the middle and eastern routes of the South-to-North Water Transfer Project (see Fig. 2) is considered.

Under the current permissive social-economic condition, about 0.3 x 10^9 m^3 of water recycling volume from the RUS is realised to increase the available amount of water supply in YRB.

The FWU measure is implemented to raise the flood limit level of Xiaolangdi Reservoir (Fig. 2) from September to October, which could add floodwater storage capability of about 2 x 10^9 m^3 and relieve tensions around water utilisation in the lower reaches of YR.

Based on the above methods, 23 groups of alternatives were set after the appropriate consultation, appraisal and assessment by the workgroup (Table 1). Five indexes were selected to evaluate the alternatives, including the available amount of water

![Figure 2](image-url)

**Figure 2**
Geographic location of Yellow River Basin and the South-to-North Water Transfer Project, China

| Alternative | WTP x 10^9 m^3 | RUS | FWU | WSI | WSA |
|-------------|----------------|-----|-----|-----|-----|
| 1           | 2              | 2   | 10  | 2   | 10  |
| 2           | 2              | 2   | 10  | 2   | 10  |
| 3           | 2              | 2   | 10  | 2   | 10  |
| 4           | 2              | 2   | 10  | 2   | 10  |
| 5           | 2              | 2   | 10  | 2   | 10  |
| 6           | 2              | 2   | 10  | 2   | 10  |
| 7           | 2              | 2   | 10  | 2   | 10  |
| 8           | 2              | 2   | 10  | 2   | 10  |
| 9           | 2              | 2   | 10  | 2   | 10  |
| 10          | 2              | 2   | 10  | 2   | 10  |
| 11          | 2              | 0.3 | 2   | 10  | 10  |
| 12          | 2              | 0.3 | 2   | 10  | 10  |
| 13          | 2              | 0.3 | 2   | 10  | 10  |
| 14          | 2              | 0.3 | 2   | 10  | 10  |
| 15          | 3              |     |     |     |     |
| 16          | 3              |     |     |     |     |
| 17          | 3              |     |     |     |     |
| 18          | 3              |     |     |     |     |
| 19          | 3              |     |     |     |     |
| 20          | 3              | 0.3 | 2   | 10  | 10  |
| 21          | 3              | 0.3 | 2   | 10  | 10  |
| 22          | 3              | 0.3 | 2   | 10  | 10  |
| 23          | 3              | 0.3 | 2   | 10  | 10  |

Note: WTP= water transfer project; RUS= recycling utilisation of sewage; FWU=floodwater utilisation; WSI=water saving by industry; WSA=water saving by agriculture.
supply, the quantity of water required, the volume of the water shortage, the environmental water requirement (quantity) and the quantity of electricity generated from multiple reservoirs in the main stream of YR (Longyangxia, Liujiaxia, Qingtongxia, Sanmenxia and Xiaoalingdi; see Fig. 2). These indexes can all be easily quantified. Therefore, a decision-making matrix $Q_{234}$ is constructed. The values of $d_1$ of the standardisation matrix $D$ are given in Table 2.

**Results and discussion**

According to the proposed approach (see the flow chart in Fig. 1) and the values of $d_1$ of standardisation matrix $D$ in Table 2, we can determine the values of normalisation matrix $P$, information entropy ($E_1$) and evaluation entropy ($e_1$), based on Eqs. (4) and (5), which are shown in Tables 3 and 4.

According to Eq. (6), the EWs are determined as $(\theta_1, \theta_2, \theta_3, \theta_4, \theta_5) = (0.2047, 0.2034, 0.1844, 0.2027, 0.2049)$. The membership degree of $P(i)$ and the subjective weight (SW) are calculated as $P(1) = 0.1000, P(2) = 0.8982, P(3) = 0.7737, P(4) = 0.6131, P(5) = 0.3869$ and $(\delta_1, \delta_2, \delta_3, \delta_4, \delta_5) = (0.2723, 0.2446, 0.2107, 0.1670, 0.1054)$, respectively, in terms of Eq. (7). The comprehensive weight (CW) can be determined based on Eq. (8): $w_1 = 0.2047$, $w_2 = 0.2034$, $w_3 = 0.1844$, $w_4 = 0.2027$, $w_5 = 0.2049$. Thus a comprehensive weight matrix $W^{(1)}_{234}$ can be built based on all the combined numbers of the 5 CWs. The $36 \times 120$ size matrix $V$ of expected value $v_1$ is also derived in terms of the product of the standardisation matrix $D_{234}$ and the transposed comprehensive weight matrix $(W^{(1)}_{234})^T$. Therefore, based on Eqs. (9) and (10), two $36 \times 120$ size matrices of observability-controllability

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**Table 2**

| Alternative | AWS | QWR | VWS | EWR | QGE |
|-------------|-----|-----|-----|-----|-----|
| 1           | 0.992 | 1.000 | 1.000 | 0.858 | 0.942 |
| 2           | 1.000 | 0.969 | 0.927 | 0.836 | 0.944 |
| 3           | 0.989 | 0.945 | 0.774 | 0.839 | 0.955 |
| 4           | 0.981 | 0.913 | 0.511 | 0.863 | 0.970 |
| 5           | 0.958 | 0.889 | 0.469 | 0.898 | 0.976 |
| 6           | 0.982 | 0.969 | 0.774 | 0.884 | 0.961 |
| 7           | 0.985 | 0.969 | 0.745 | 0.876 | 0.963 |
| 8           | 0.973 | 0.945 | 0.603 | 0.881 | 0.972 |
| 9           | 0.761 | 0.913 | 0.376 | 0.916 | 0.989 |
| 10          | 0.038 | 0.889 | 0.336 | 0.952 | 0.998 |
| 11          | 0.088 | 0.854 | 0.716 | 0.870 | 0.959 |
| 12          | 0.795 | 0.930 | 0.582 | 0.884 | 0.978 |
| 13          | 0.963 | 0.898 | 0.354 | 0.912 | 0.992 |
| 14          | 0.940 | 0.873 | 0.313 | 0.954 | 0.998 |
| 15          | 0.977 | 0.954 | 0.657 | 0.897 | 0.970 |
| 16          | 0.978 | 0.954 | 0.649 | 0.894 | 0.963 |
| 17          | 0.958 | 0.930 | 0.586 | 0.924 | 0.976 |
| 18          | 0.945 | 0.898 | 0.361 | 0.959 | 0.992 |
| 19          | 0.922 | 0.873 | 0.320 | 0.995 | 0.998 |
| 20          | 0.979 | 0.954 | 0.640 | 0.894 | 0.963 |
| 21          | 0.963 | 0.930 | 0.541 | 0.919 | 0.981 |
| 22          | 0.947 | 0.898 | 0.349 | 0.957 | 0.994 |
| 23          | 0.924 | 0.873 | 0.307 | 1.000 | 1.000 |

**Note:** AWS=available amount of water supply; QWR=quantity of water required; VWS=volume of water shortage; EWR=environmental water requirement; QGE=quantity of electricity generated from the multi-reservoir system.

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**Table 3**

| Alternative | AWS | QWR | VWS | EWR | QGE |
|-------------|-----|-----|-----|-----|-----|
| 1           | 0.2070 | 0.2087 | 0.2087 | 0.1790 | 0.1966 |
| 2           | 0.2139 | 0.2072 | 0.1982 | 0.1788 | 0.2019 |
| 3           | 0.2197 | 0.2099 | 0.1719 | 0.1864 | 0.2121 |
| 4           | 0.2315 | 0.2154 | 0.1206 | 0.2036 | 0.2289 |
| 5           | 0.2286 | 0.2122 | 0.1119 | 0.2143 | 0.2329 |
| 6           | 0.2149 | 0.2120 | 0.1694 | 0.1934 | 0.2103 |
| 7           | 0.2171 | 0.2135 | 0.1642 | 0.1930 | 0.2122 |
| 8           | 0.2225 | 0.2160 | 0.1379 | 0.2014 | 0.2222 |
| 9           | 0.2133 | 0.2197 | 0.0905 | 0.2205 | 0.2380 |
| 10          | 0.2281 | 0.2161 | 0.0817 | 0.2315 | 0.2426 |
| 11          | 0.2202 | 0.2126 | 0.1596 | 0.1939 | 0.2137 |
| 12          | 0.2242 | 0.2138 | 0.1338 | 0.2033 | 0.2249 |
| 13          | 0.2338 | 0.2180 | 0.0859 | 0.2214 | 0.2408 |
| 14          | 0.2305 | 0.2141 | 0.0768 | 0.2339 | 0.2447 |
| 15          | 0.2193 | 0.2141 | 0.1475 | 0.2013 | 0.2177 |
| 16          | 0.2201 | 0.2147 | 0.1458 | 0.2012 | 0.2181 |
| 17          | 0.2190 | 0.2126 | 0.1340 | 0.2112 | 0.2231 |
| 18          | 0.2274 | 0.2161 | 0.0869 | 0.2308 | 0.2387 |
| 19          | 0.2244 | 0.2125 | 0.0779 | 0.2422 | 0.2429 |
| 20          | 0.2210 | 0.2153 | 0.1445 | 0.2018 | 0.2174 |
| 21          | 0.2222 | 0.2146 | 0.1248 | 0.2120 | 0.2263 |
| 22          | 0.2285 | 0.2166 | 0.0842 | 0.2309 | 0.2398 |
| 23          | 0.2251 | 0.2127 | 0.0748 | 0.2437 | 0.2437 |
of increasing water resource availability and reducing water input and output is also different. However, from the viewpoint and related industries. In addition, the relationship between ison between the 5 methods because of their different contexts resource problems in YRB. It is difficult to carry out a compar

Figure 3
Changing trends of average observability-controllability risk ($R_{oc}$) and gain by comparison ($G_{bc}$)

For example, to analyse the influence of the RUS measure, the comparison between A7 and A11, or A8 and A12, A9 and A13, A10 and A14, should be carried out. Results show that the difference between $R_{oc}$ and $G_{bc}$ is approximate in the case of the same methods, of WTP, FWU, WSI and WSA. This means that the RUS method has a small degree of influence on the results. In a similar way, by the comparison between A1 and A2, or A6 and A7, A15 and A16, the degree of difference between $R_{oc}$ and $G_{bc}$ is also not distinct under the same conditions (with the methods WTP, RUS, WSI and WSA), which shows that the FWU method does not have an important effect on the results. The $G_{bc}$ of A2, in particular, is much smaller than that of A1. From the comparison between A6 and A15 (both alternatives only involve WTP), the values of $R_{oc}$ and $G_{bc}$ are rather small. On the basis of the analysis between A5, A10, A14, A19 and A23, if a certain alternative consists of both WSI and WSA, the values of $R_{oc}$ and $G_{bc}$ will be close to the largest. A1 is a basic and comparative alternative which does not involve any of the available methods/ measures (WTP, RUS, FWU, WSI or WSA) and its priority-ranked order of $G_{bc}$ is 15 (see Fig.4), which is larger than that of A2, A3, A6, A7, A11, A15, A16 and A20. This indicates that these alternatives are rather disadvantageous due to the absence of any water-saving measures in agriculture (WSA). At the same time, based on the comparison among A5, A10 and A19, we see that the greater the water volume transferred from the middle and eastern routes of the South-to-North Water Transfer Project, the greater the values of $R_{oc}$ and $G_{bc}$. Therefore, according to the analysis of different measures, a priority-ranked order of decision measures can be achieved as: WSA$>$WTP$>$WSI$>$RUS$>$FWU. This indicates that the WSA method/measure has the most important positive influence on the results.

Conclusions

This study presents a comprehensive entropy weight observability-controllability risk analysis approach to decision-making for alternatives and measures in water resource planning of

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the Yellow River Basin, China. Results demonstrate that the approach provides a new analysis method for the decision field of water resource planning.

According to the relationship between \( R_{oc} (x) \) and \( G_{bc} (y) \) shown in Fig. 4, there is a best-fit curve of \( y = 2.5925x^2 + 0.2773x + 1.016 \) with a high degree of correlation \( (R^2 = 0.964) \). The \( G_{bc} (y) \) is in direct proportion to the \( R_{oc} (x) \). At the point on the curve with coordinates \((0.2566, 0.9886)\) the maximal slope \( K_{\text{max}} = 1.053 \), indicating the most optimal point. If the real allowable value of risk is considered and set as a certain value, such as \( R_{oc} \), only the alternative with the shortest distance of point \((R_{oc}, G_{bc})\) to the optimisation point \( (0.2566, 0.9886) \), and satisfying the condition of \( R_{oc} \leq R_{oc} \) could be adopted as the optimal one. In addition, a priority-ranked order of measures can be achieved as: WSA>WTP>WSI>RUS>FWU in terms of the comparison of those alternatives with the same measures or without a certain measure.

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