\[ \eta \text{ photoproduction off the deuteron and low-energy } \eta\text{-nucleon interaction} \]

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(Received December 25, 2018)

We study \( \eta \) photoproduction off the deuteron (\( \gamma d \rightarrow \eta pn \)) at a special kinematics: \( \sim 0.94 \) GeV of the photon beam energy and \( \sim 0^\circ \) of the scattering angle of the proton. This kinematics is ideal to extract the low-energy \( \eta \)-nucleon scattering parameters such as \( a_{\eta N} \) (scattering length) and \( r_{\eta N} \) (effective range) because the \( \eta \)-nucleon elastic scattering is significantly enhanced. We show that if a ratio \( R \), the \( \gamma d \rightarrow \eta pn \) cross section divided by the \( \gamma p \rightarrow \eta p \) cross section convoluted with the proton momentum distribution in the deuteron, is measured with \( 5\% \) error, \( \text{Re}[a_{\eta N}] \) (\( \text{Re}[r_{\eta N}] \)) can be determined at the precision of \( \sim \pm 0.1 \text{ fm} \) (∼ \( \pm 0.5 \text{ fm} \)), significantly narrowing down the currently estimated range of the parameters. The measurement is ongoing at the Research Center for Electron Photon Science (ELPH), Tohoku University.

**KEYWORDS:** meson photoproduction, hadron-hadron interaction, \( \eta \)-mesic nuclei

1. Introduction

The low-energy \( \eta \)-nucleon interaction can be characterized with two parameters, the scattering length \( a_{\eta N} \) and effective range \( r_{\eta N} \). The existence of exotic \( \eta \)-mesic nuclei largely depends on \( a_{\eta N} \) that determines the attractive or repulsive nature of the low-energy \( \eta N \) interaction [1]. However, \( a_{\eta N} \) has not been well determined yet. Previous works have attempted to extract \( a_{\eta N} \) and \( r_{\eta N} \) by analyzing the \( \pi N \rightarrow \pi N, \eta N \) and \( \gamma N \rightarrow \pi N, \eta N \) reaction data [1], and also the \( pn \rightarrow \eta d \) reaction data [2]. These analyses gave fairly consistent results for the imaginary parts of \( a_{\eta N} \) and \( r_{\eta N} \) which are within \( \text{Im}[a_{\eta N}] = 0.2–0.3 \text{ fm} \) and \( \text{Im}[r_{\eta N}] = -1–0 \text{ fm} \), respectively [1]. However, their real parts are not well-determined: \( \text{Re}[a_{\eta N}] = 0.2–0.9 \text{ fm} \) and \( \text{Re}[r_{\eta N}] = -6 \) to \( +1 \text{ fm} \). The large model-dependence in the real parts stems from the difficulty of isolating the \( \eta N \) scattering amplitudes from other mechanisms involved in the reactions analyzed.

An ongoing \( \eta \) photoproduction experiment [3] at the Research Center for Electron Photon Science (ELPH), Tohoku University is designed to overcome the difficulty of determining \( a_{\eta N} \) by utilizing a special kinematics. In this experiment, a photon beam with \( E_{\gamma} \sim 0.94 \text{ GeV} \) hits a deuteron target and the recoil proton from \( \gamma d \rightarrow \eta pn \) is detected at \( \theta_p \sim 0^\circ \). At this kinematics, an \( \eta \) produced from a quasi-free proton is almost at rest, and thus it would interact strongly with the spectator neutron. On the other hand, the struck proton goes away with a large momentum, and thus it would not interact with the \( \eta \) and neutron. This seems an ideal kinematical condition, referred to as the ELPH kinematics, to determine the low-energy \( \eta N \) scattering parameters. The present theoretical analysis [4] will show that a combined cross-section data for \( \gamma d \rightarrow \eta pn \) and \( \gamma p \rightarrow \eta p \) expected to be taken in the ELPH experiment would indeed lead to significant reduction of the current uncertainty of \( a_{\eta N} \) and \( r_{\eta N} \).
processes. The model must be built with reliable amplitudes for elementary and \( \eta N \) background contributions. Regarding so, we can reliably isolate the amplitude for the \( \eta \pi \) unitary model for the \( \pi \) generated with a dynamical coupled-channels (DCC) model [5, 6]. The DCC model is a multichannel 27∼[Fig. 1(a)], \( \pi \) contains the first-order rescattering mechanisms as illustrated in Fig. 1. The figure taken from Ref. [4]. Copyright (2017) APS

2. Model

We study \( \gamma d \rightarrow \eta nn \) relevant to the ELPH experiment with a model based on the impulse and the first-order rescattering mechanisms as illustrated in Fig. 1. The \( \eta \)-exchange mechanism [Fig. 1(b)] contains the \( \eta N \rightarrow \eta N \) subprocess we are interested in, while the other mechanisms (the impulse [Fig. 1(a)], \( \pi \)-exchange [Fig. 1(c)], and \( NN \)-rescattering [Fig. 1(d)] mechanisms) are background processes. The model must be built with reliable amplitudes for elementary \( \gamma N \rightarrow MN, MN \rightarrow M'N \), and \( NN \rightarrow NN \) processes with \( M'\) = \( \pi, \eta \), as well as with a realistic deuteron wave function. By doing so, we can reliably isolate the amplitude for the \( \eta N \rightarrow \eta N \) subprocess from data using well-predicted background contributions. Regarding \( \gamma N \rightarrow MN \) and \( MN \rightarrow M'N \) amplitudes, we employ those generated with a dynamical coupled-channels (DCC) model [5, 6]. The DCC model is a multichannel unitary model for the \( \pi N \) and \( \gamma N \) reactions in the nucleon resonance region. It was constructed fitting ~ 27,000 data points, and successfully describes [5, 6] \( \pi N \rightarrow \pi N, \pi \pi N, \eta N, \Lambda K, \Xi K \) and \( \gamma N \rightarrow \pi N, \pi \pi N, \eta N, \Lambda K, \Xi K \) reactions over the energy region from the thresholds up to \( \sqrt{s} \approx 2.1 \) GeV. For example, the DCC model describes \( \gamma p \rightarrow \eta p \) differential cross sections in a very good agreement with data over the energy region relevant to the following calculations of \( \gamma d \rightarrow \eta n \). This confirms that the most important \( \gamma p \rightarrow \eta p \) amplitudes among the elementary amplitudes for describing \( \gamma d \rightarrow \eta pn \) have been well tested by the data. This DCC model predicts the \( \eta N \) scattering parameters to be \( a_{\eta N} = 0.75 + 0.26i \) fm and \( r_{\eta N} = -1.6 - 0.6i \) fm, which are consistent with the previously estimated ranges. As for the deuteron wave function and the \( NN \) scattering amplitudes, we use the CD-Bonn potential [7] to generate them.

3. Result

We can make a parameter-free prediction for the \( \gamma d \rightarrow \eta pp \) cross sections using the model described above. We can thus assess the validity of the model by confronting our model predictions with existing data. In Fig. 2(left), we show \( d\sigma/d\Omega_\eta \) at \( E_\gamma = 775 \) MeV from our DCC-based model with and without the rescattering contributions along with the data. Our parameter-free prediction is found to be in an excellent agreement with the data. The \( \eta N \rightarrow \eta N \) rescattering gives a slight enhancement in the backward direction, which is important for this nice agreement. A similar DCC-based model for \( \gamma d \rightarrow \pi NN \) [9, 10] also gives predictions that agree well with data by taking account of significant rescattering effects.

We now move on to the \( \gamma d \rightarrow \eta pp \) reaction at the ELPH kinematics (\( E_\gamma = 0.94 \) GeV and \( \theta_p = 0^\circ \)). In Fig. 2(right-top), the predicted threefold differential cross section, \( d^3\sigma/dM_{\eta p}d\Omega_p \), are presented as a function of the \( \eta \)-neutron invariant mass \( M_{\eta p} \). The impulse mechanism [Fig. 1(a)] including the \( \gamma p \rightarrow \eta p \) (\( \gamma n \rightarrow \eta n \)) amplitudes gives the dominant (negligible) contribution. A substantial contribution is from the \( \eta \)-exchange mechanism [Fig. 1(b)], and the cross sections including the impulse mechanisms only are changed by −40 to +20% [difference between the dashed and dotted
Fig. 2. [Left] Predicted differential cross sections for $\gamma d \rightarrow \eta pn$. The dotted curve is from the impulse approximation, and the solid curve includes rescattering mechanisms in addition. The data are from Ref. [8]. [Right-Top] Differential cross section for $\gamma d \rightarrow \eta pn$ at $E_\gamma = 0.94$ GeV and $\theta_p = 0^\circ$. The impulse approximation (dotted curve), the impulse and $\eta$-exchange mechanisms (dashed curve), the impulse, $\eta$- and $\pi$-exchange mechanisms (dash-dotted curve), and the full calculation (solid curve). [Right-Bottom] Ratios of the differential cross sections by Ref. [4]. Copyright (2017) APS

curves in Fig. 2(right-bottom)]. The $\pi$-exchange [Fig. 1(c)] contribution is smaller, suppressing the cross sections by \( \lesssim 9\% \) (difference between the dashed and dash-dotted curves). The $NN$ rescattering [Fig. 1(d)] contribution (deviation of the dash-dotted curve from 1) is very small for $M_{pn} \lesssim 1.5$ GeV. This feature is what we expect to find in this special kinematics, and indicates that the proton essentially does not interact with the $\eta n$ system. Thus multiple rescatterings beyond the first-order rescattering [Figs. 1(b)–1(d)] should be safely neglected for $M_{pn} \lesssim 1.5$ GeV. We have also examined an off-shell momentum effect associated with the $\eta n \rightarrow \eta n$ scattering amplitude and found it very small. Because we are interested in a $M_{pn}$ region close to the threshold, higher partial waves for the $\eta n \rightarrow \eta n$ amplitudes are negligible. Therefore, we modify the full $\gamma d \rightarrow \eta pn$ model by replacing the $\eta n$ scattering amplitude with the $S$-wave one parametrized with $a_{\eta N}$ and $r_{\eta N}$. These scattering parameters are determined by analyzing the forthcoming ELPH data.

The ELPH data will be given in a form of the ratio, denoted by $R_{\text{expt}}$, of the measured cross sections for $\gamma d \rightarrow \eta pn$ divided by those for $\gamma p \rightarrow \eta p$ convoluted with the proton momentum distribution in the deuteron. This is for removing systematic uncertainties of the acceptance from the detector coverage. Therefore, from the theoretical side, we need to calculate the corresponding quantity given by

$$R_{\text{th}}(M_{pn}) = \frac{d^3 \sigma_{\text{full}} / dM_{pn} d\Omega_p |_{\theta_p = 0^\circ}}{d^3 \sigma_{\text{imp}} / dM_{pn} d\Omega_p |_{\theta_p = 0^\circ}},$$

where $\sigma_{\text{full}}$ ($\sigma_{\text{imp}}$) is calculated with the full model (the impulse term only). Now the question is how sensitive $R_{\text{th}}$ is against changing $a_{\eta N}$ and $r_{\eta N}$. Also, we are interested in what is the required precision of $R_{\text{expt}}$ for significantly reducing the current uncertainties of $a_{\eta N}$ and $r_{\eta N}$.

First Re[$a_{\eta N}$] is changed over $0.2 - 1.0$ fm, with Im[$a_{\eta N}$] = 0.25 fm and $r_{\eta N}$ = 0 fm being fixed. The resulting cross sections cover the red striped region as shown in Fig. 3(top), within the considered ELPH kinematics and $M_{pn} \leq 1.505$ GeV. The ratio $R_{\text{th}}$ also changes accordingly as shown in Fig. 3(bottom); $R_{\text{th}}$ shows more clearly the sensitivity to the variation of Re[$a_{\eta N}$]. The cross section and thus $R_{\text{th}}$ changes by \( \sim 25\% \) at the quasi-free (QF) peak position of $M_{pn} \sim 1.488$ GeV, as indicated
by the width of the striped band. We also show the green solid bands that have the widths of $\pm 5\%$ at the QF peak. This green band is covered by our model when $\text{Re}[a_{\eta N}]$ is varied by $\pm 0.1\text{ fm}$ from 0.6 fm. This means that $R_{\text{expt}}$ data of $5\%$ error per MeV bin can determine $\text{Re}[a_{\eta N}]$ at the precision of $\sim \pm 0.1\text{ fm}$, significantly reducing the currently estimated range. Data of $R_{\text{expt}}$ with this precision is expected to be taken in the ongoing ELPH experiment [3].

Next $\text{Re}[r_{\eta N}]$ is varied over $-6 \rightarrow 0 \text{ fm}$ which is the currently estimated range, while the scattering length being fixed at the value from the latest DCC analysis [6], $a_{\eta n} = 0.75 + 0.26i\text{ fm}$ and $\text{Im}[r_{\eta N}] = 0\text{ fm}$. Accordingly, the cross section and $R_{th}$ change over the red striped region in Fig. 4. The effect of changing $r_{\eta N}$ is visible at $-5\text{ MeV}$ above the $\eta N$ threshold. The ratio $R_{th}$ at $M_{\eta n} = 1.5\text{ GeV}$ changes by $\sim 30\%$ ($\sim 5\%$) when $\text{Re}[r_{\eta N}]$ is changed over $-6 \rightarrow 0 \text{ fm}$ ($-3.5 \sim -2.5\text{ fm}$) as indicated by the red striped (green solid) band. Therefore, $\text{Re}[r_{\eta N}]$ at the precision of $\lesssim \pm 0.5\text{ fm}$, which is significantly improved precision over the current estimates, can be obtained by measuring $R_{\text{expt}}$ data of $5\%$ error per MeV bin.

Acknowledgments

This work is in part supported by Fundação de Amparo à Pesquisa do Estado de São Paulo (FAPESP), Process No. 2016/15618-8, and by JSPS KAKENHI Grant Number JP18K03632.

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