Contactless Excitation of Acoustic Resonance in Thin Wafers

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(Dated: July 26, 2022)

Contactless excitation and detection of high harmonic acoustic overtones in a thin single crystal are described using radio frequency spectroscopy techniques. Single crystal [001] silicon wafer samples were investigated, one side covered with a Nb thin film, the common starting point for fabrication of quantum devices. The coupling between electromagnetic signals and mechanical oscillation is achieved from the Lorentz force generated by an external magnetic field. This method is suitable for any sample with a metallic surface or covered with a thin metal film. High resolution measurements of the temperature dependence of the sound velocity and elastic constants of silicon are reported and compared with previous work.

INTRODUCTION

Quantum devices essential in quantum information technology, are fabricated on silicon or sapphire wafers. In recent work it was discovered that acoustic modes in the wafer can play an important role in quantum state manipulation, including swap operations between acoustic and transmon qubit states resulting in cooling[1, 2].

The acoustic modes are generated from piezoelectric transducers prepared on the wafer. This is generically the most common method for acoustic investigation of materials, wherein electrodes are bonded to transducers that are in direct contact with the samples of interest. The piezoelectric response of the transducer to an oscillating voltage converts the electromagnetic signal to mechanical oscillation. In some circumstances it is undesirably or impractical to have the electrodes or transducers in physical contact with the sample. Here we have developed a contactless technique for generating and measuring the acoustic resonances in materials.

Dobbs[3] describes generating acoustic resonances in metals with a solenoid and a static magnetic field. The coupling between electromagnetic signals and mechanical oscillation is achieved by the Lorentz force generated by the magnetic field, which sidesteps the use of piezoelectric materials. The Lorentz force occurs at the surface of the metal, or within the radio frequency (RF) penetration depth, generating acoustic modes in the bulk. With this approach we have studied high overtone acoustic modes in silicon wafers and made precise measurements of both longitudinal and transverse sound velocities and calculated the corresponding elastic constants.

METHODS

Our sample is a piece of [001] single crystal silicon wafer with one side covered with a Nb thin film. The dimension of the sample cut from a commercial wafer originally 15 cm in diameter, is 4mm x 4mm x 330µm (float-zone > 10,000Ωcm). The results described in detail in this work are for a Nb film, 155 nm thick, produced by HIPIMS sputtering at Rigetti Computing. High magnetic field susceptibility measurements up to 14T indicate that there are no magnetic impurities, either before or after adding the Nb film. Additionally, we have investigated similar samples from the National Institute of Science and Technology and quartz transducers from Boston Piezo-Optics Inc. The radio frequency (RF) setup for contactless acoustic investigation that we report here, is the same as that commonly used for pulsed nuclear magnetic resonance (NMR) experiments. The sample is inserted in an RF coil that generates local RF fields, $H_1$, typically of order or less than 0.01 T and placed in the magnetic field of a highly homogeneous superconducting magnet ranging from 7 to 14 T. The RF coil provides high frequency RF pulses from the NMR spectrometer. Reciprocally, after an excitation pulse, the acoustic resonances in the sample induce electromagnetic radiation that we detect with the same coil. This signal is processed by complex Fourier transformation to give a spectrum after minimal signal averaging for less than 10 minutes. We report on measurements of the spectral characteristics of the high harmonic acoustic signals under different conditions of pulsed excitation, frequency, magnetic field, and temperature from which transverse and longitudinal sound speeds were determined and the elastic constants of single crystal silicon were determined.

The protocol for excitation and detection of an acoustic resonance is very similar to the procedure for single-pulse, free-induction-decay, NMR measurements with the notable exception that the direction of the RF field need not be perpendicular to the externally applied field. First, an RF pulse of a few microseconds is applied to the coil which excites an induced current sheet perpendicular to the RF field in the Nb film, depicted in Fig. 1. Since
the Nb film is in an external magnetic field, the Faraday induced oscillating current in the film gives rise to an oscillating Lorentz force acting on the Nb film, causing the Nb film to oscillate producing either transverse or longitudinal acoustic modes propagating normal to the plane of the wafer. The acoustic mode selection is determined by the relative orientation of the external field $H_0$ to that of the RF coil $H_1$. The acoustic wave is reflected from the other side of the crystal, forming an acoustic standing wave if the excitation frequency is on resonance with the natural frequency of the silicon wafer or one of its harmonics. The two orientations of the sample are shown in Fig. 1(a) and (b). For other orientations, mixed modes would be expected.

During the detection period following the RF pulse, the induced current in the Nb film disappears leaving spectra with sharply-defined harmonic content, Fig. 2. Induced acoustic signals observed in NMR experiments are often a nuisance especially with piezoelectric samples where the excitation is from the RF voltage. The latter can be mitigated by inserting a metal foil within the RF coil which is not required in the present work and which we have independently shown does not effect the results we describe here.

**EXPERIMENT RESULTS**

First, the acoustic spectra for various harmonics were measured. The $n^{th}$ harmonic frequency of the acoustic resonance in the silicon wafer is given by:

$$f_n = \frac{nv}{2d}$$

where $v$ and $d$ represent the sound velocity and the thickness of the silicon wafer respectively. The acoustic signal only occurs when the resonance frequency is in the excitation bandwidth of the pulse, typically of the order of 1 MHz. A Fourier transformation of the time-domain signal following the excitation pulse gives rise to an acoustic resonance peak in the frequency domain, as shown in Fig. 2(a). To cover a broad range of frequency the RF frequency of the pulse is shifted in steps over the desired range. The excitation amplitude was measured independently and the tuning of the RF tuned circuit was adjusted for each step.

In Fig. 2(b), the data points were obtained from a first moment analysis of the spectra. The error bars of the moment analysis are smaller than the size of the data points. The two linear fit lines go to zero with very little uncertainty, confirming that the signals are acoustic in origin.

Factors that affect the intensity of the signal were also investigated. We found that the signal intensity mainly depends on the pulse length, the pulse voltage, and the external field, with the pulse frequency set to the peak frequency of the spectral harmonic. The results are shown in Fig. 3. The intensities were obtained from the integral of the spectrum and the error bars are also negligible.

According to the calculation by Dobbs, the acoustic amplitude is proportional to the RF field, as might be expected. Therefore, the signal intensity, which is proportional to the acoustic amplitude should be proportional to the rf pulse voltage, which is proportional to the rf field. The linear fit in the inset of Fig. 3(a) shows linear dependence between the signal intensity and the pulse voltage, consistent with the theory.

From Fig. 3(b) we can see that the signal intensity has a positive correlation with the pulse length. This can be understood by the fact that for longer pulse lengths,
more energy is transferred to the sample, resulting in a larger amplitude of harmonic oscillation. However, this relationship is non-linear, and it is reasonable to assume that for a long pulse length, the amplitude will reach an equilibrium value, with a characteristic time of 22.6 µs, given by an exponential fit.

The external field plays a role for both excitation and detection. Since the coupling strength between electromagnetic and mechanical oscillation is proportional to the external field, we expect that the field dependence of the acoustic signal should be quadratic \[4\]. Our measurements in Fig. 4 are consistent with quadratic behavior.

**APPLICATION**

The technique of exciting acoustic resonance in small devices without contact has a number of potential applications. One of them is to measure the sound velocity and the elastic constants. Our measurements of the temperature dependence of sound velocities and elastic constants of a [001] silicon single crystal are shown in Fig. 5.

The sound velocities were obtained by measuring the temperature dependence of the harmonic frequency at a certain harmonic number. For the transverse measurement in Fig. 5 we used \(n = 16\) and for the longitudinal measurement, \(n = 11\). The sound velocity was then calculated from the equation \(v = 2df_n/n\), where \(d = 330 \mu m\) is the thickness of the silicon wafer. The temperature dependence of the thickness of the sample is taken into account in the calculation, with the data from Endo et al. \[9\].

The elastic constants were also calculated from the sound velocities and the density of silicon. All of our measured sound velocities are for propagation in the [001] direction. Expressions for \(C_{11}\) and \(C_{44}\) are given in Ref. \[8\].

\[
C_{11} = \rho v_l^2 \\
C_{44} = \rho v_t^2
\]

where \(\rho\) is the density of silicon, and \(v_l\) and \(v_t\) are the longitudinal and transverse sound velocities respectively. The temperature dependence of the density is also taken into account in the calculation, with the data from Endo et al. work \[9\]. The results are shown in Fig. 5(c) and (d).
The dashed lines in the figures are obtained by fitting the data with an empirical equation given by Wachtman et al. [5], useful in describing the temperature dependence of elastic constants in crystals. Our results are compared with those of McSkimin [6] given in the insets to Figs. 2(c) and (d), who also measured the temperature dependence of $C_{11}$ and $C_{44}$ of silicon. Our measurements have the same trend as theirs. However, our values are $\approx 6\%$ larger, a difference of a factor of six larger than our error of $1\%$ which is attributable to the systematic error in our measurement of the wafer thickness at room temperature.

**SUMMARY**

We have developed a new technique of contactless excitation of acoustic resonances suitable for characterization of single crystals with a metallic surface, such as the silicon wafers used in quantum device applications. This could be performed at various stages of device fabrication since the method is contactless. We note that in Ref. [2] the alternative method of contact with a piezoelectric transducer was used to produce high harmonic acoustic signals in a wafer on which a transmon had been fabricated. At mK-temperatures these acoustic modes are in the quantum limit. If stochastic excitation of acoustic modes plays a role in limiting qubit coherence, our method can provide a useful noninvasive characterization tool. The contactless technique should also be applicable to investigate metallic samples of quantum materials where there is coupling between magnetic degrees of freedom and high Q acoustic modes. In this instance the RF field generates a Lorentz force limited to an RF penetration depth complementary to the acoustic modes that penetrate throughout.

The required setup for the technique is an RF circuit and an external magnetic field, similar to that used in traditional pulsed NMR experiments where excitation and detection are performed with the same coil. The frequencies of the harmonics and the thickness of the sample determine the sound velocities and mode selection is determined by sample orientation. The detected signal intensity is proportional to the RF pulse amplitude and the square of the external magnetic field. With this technique, in the present work, the temperature dependence of both transverse and longitudinal sound velocities, as well as the elastic constants, have been precisely measured in a [001] silicon wafer where the precision is that of the frequency of the acoustic modes in the temperature range of 20 - 290 K.

**ACKNOWLEDGMENT**

We thank Anna Grassellino, Alex Romanenko, Jens Koch, Man Nguyen, John Scott, and Daehan Park for useful discussion and comments. This work was supported by the U.S. Department of Energy, Office of Science, National Quantum Information Science Research Centers, Superconducting Quantum Materials and Systems Center (SQMS) under contract No. DE-AC02-07CH11359.

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