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A. Youssef

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Infrared behavior and gauge artifacts in de Sitter spacetime

I. The photon field

A. Youssef

Université Paris Diderot Paris 7, Laboratoire APC, Bâtiment Condorcet, Case 7020, 75205 Paris Cedex 13, France

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We study the infrared (long distance) behavior of the free photon field in de Sitter spacetime. Using a two-parameter family of gauge fixing terms, we show that the infrared (IR) behavior of the two-point function is highly gauge-dependent and ranges from vanishing to growing. This situation is in disagreement with its counterpart in flat spacetime, where the two-point function vanishes in the IR for any choice of the gauge fixing parameters. A criterion to isolate the “physical” part of the two-point function is given and is shown to lead to a well-behaved two-point function in the IR.

INTRODUCTION

The study of quantum field theory in the de Sitter background is of paramount importance to the understanding of the early universe as well as its present accelerated expansion. One of the most striking, yet poorly understood, aspects of de Sitter QFT is the so-called infrared problem. The simplest and most serious manifestation of this problem being the non-vanishing of the correlation functions for largely - spacelike and timelike -separated points. This is for instance a well-known fact for the massless minimally coupled (mmc) scalar and the graviton fields. In this letter we study the IR behavior of the photon field in de Sitter space and show that it exhibits similar IR pathologies. More importantly we are able to show that these are purely gauge artifacts.

The organization of the letter is as follows. First we compute the correlation function using the parallel propagator $W_{\alpha\bar{\alpha}}(x, x')$ between $x$ and $x'$, and the two vectors $n_a = \nabla_a \mu$ and $n_a' = \nabla_a' \mu$. Our two-point function is thus written as

$$W_{\alpha\bar{\alpha}}(x, x') = \alpha_1(\mu)g_{\alpha\bar{\alpha}} + \alpha_2(\mu)n_{\alpha}n_{\bar{\alpha}}$$

where, for spacelike separations ($\mu^2 > 0$), $\alpha_1$ and $\alpha_2$ are scalar functions of the geodesic distance $\mu$ only. We will frequently use the following formulas:

$$g_{\alpha}\ n_{\bar{\alpha}} = -n_{\alpha}' , \qquad g_{ab} = g_{a'}g_{b'}$$

$$\nabla_{\bar{a}} n_b = A(g_{ab} - n_{a}n_{b}) , \quad \nabla_a n_{\bar{b}} = C(g_{ab} + n_{a}n_{b})$$

where

$$A = \cot(\mu/R) , \quad C = -\csc(\mu/R)/R .$$

It is also useful to introduce the quantity $z$ given for spacelike separations ($\mu^2 > 0$ or $0 < z < 1$) by

$$z = \cos^2 \left( \frac{\mu}{2R} \right) . \quad (1)$$

All of our calculations are performed in the spacelike region $0 < z < 1$. They can be extended further by analytic continuation in the $z$ variable to the cut complex plane $\mathbb{C} \setminus (1, \infty)$. Finally, the Feynman propagator $G_{\alpha\bar{\alpha}}^{F} = i\langle \Omega | T A_{\alpha}(x)A_{\bar{\alpha}}(x') | \Omega \rangle$, can be obtained as the limiting value of $W_{\alpha\bar{\alpha}}$ when approaching the branch cut $z > 1$ from above.

We end our introduction by noting that several, quite interesting, recent works (see among many others) were devoted to the study of infrared effects in de Sitter. In these articles however, only massive (although interacting) fields are considered. IR pathologies are of course much stronger for massless fields and they appear already at the linear level.

*ahmed.youssef@apc.univ-paris7.fr
The gauge fixed action describing the massless vector field $A_a$ is

$$S_A = \int d^4x \sqrt{-g} \left( \frac{1}{4} F_{ab} F^{ab} + \frac{\lambda}{2} (\nabla_a A^a)^2 \right)$$  \hspace{1cm} (2)$$

where $F_{ab} = \nabla_a A_b - \nabla_b A_a$. The resulting equation of motion is $D_{ab} A^b = 0$ where

$$D_{ab} = g_{ab} \mathbb{D} - (d-1) g_{ab} + (\lambda - 1) \nabla_a \nabla_b.$$  \hspace{1cm} (3)$$

**Flat space.** In flat space ($R \to \infty$), the Fourier transform of the Feynman propagator reads

$$G_{aa'}^F(k) = \frac{1}{k^2 - i\epsilon} g_{aa'} + \frac{1 - \lambda}{\lambda} \left( \frac{k^2}{(k^2 - i\epsilon)^2} \right) k_a k_{a'}.$$$$

Using the (massless limit) of the scalar Feynman propagator (given, as always, for spacelike separations)

$$G^F(x, x') = \int \frac{d^4k}{(2\pi)^4} \frac{e^{i(k \cdot (x - x'))}}{k^2 + m^2 - i\epsilon} = \frac{i m}{(2\pi)^2} K_0(m \mu)$$  \hspace{1cm} (4)$$

(where $K$ is the modified Bessel function of the second kind) and its derivatives with respect to $x$ and $x'$ we get the coordinate-space two-point function

$$W_{aa'} = \left[ \frac{\lambda + 1}{8\pi^2 \lambda \mu^2} + \frac{1 - \lambda}{4\pi^2 \lambda \mu^2} \right] n_a n_{a'}.$$  \hspace{1cm} (5)$$

For all values of $\lambda$, this expression vanishes for large timelike and spacelike separations as expected.

**De Sitter space.** Following [10], we write the two-point function in de Sitter space as

$$W_{aa'}^{[\lambda]}(x, x') = \alpha_1^{[\lambda]}(z) g_{aa'} + \alpha_2^{[\lambda]}(z) n_a n_{a'}.$$  \hspace{1cm} (6)$$

where $\alpha_1, \alpha_2$ are scalar functions of the invariant quantity $z$ defined in [11]. The equation of motion $D_{ab} W_{aa'} = 0$ implies two independent equations on $\alpha_1$ and $\alpha_2$. These equations are most easily solved in the Feynman gauge $\lambda = 1$ and the result is found in [11] to be

$$\alpha_1^{[\lambda=1]}(z) = \frac{1}{48\pi^2 R^2} \left[ \frac{3}{1 - z} + z + \left( \frac{2}{z} + \frac{1}{z^2} \right) \ln(1 - z) \right]$$

$$\alpha_2^{[\lambda=1]}(z) = \frac{1}{24\pi^2 R^2} \left[ \frac{1}{1 - z} + \left( \frac{1}{z} - \frac{1}{z^2} \right) \ln(1 - z) \right]$$

Instead of vanishing for largely separated points, the correlation goes to a non-zero constant function

$$\lim_{z \to \infty} W_{aa'}^{[\lambda=1]}(x, x') = \frac{1}{24\pi^2 R^2} n_a n_{a'}.$$  \hspace{1cm} (7)$$

This constant vanishes in the flat spacetime limit ($R \to \infty$) as expected. The non-vanishing of the correlator in de Sitter space seems to contradict our experience with the more familiar flat space QFT. It is indeed a general result of the latter, sometimes referred to as the cluster decomposition principle [11], that the correlation functions must decay in the IR. To our knowledge, only very special QFT models, e.g. confinement models like the massless scalar in two-dimensional flat space, seem to escape this result.

As explained in the introduction, it turns out that this IR pathological behavior of the photon field is typical of de Sitter massless fields. The most notable examples are the mmc scalar and the graviton fields. The correlation functions of these fields exhibit even stronger pathologies as they grow in the IR (see for instance [12], [13], [14], [15]).

This “IR problem” is at the heart of an open discussion in the community. It led some authors [12] to speak of a “striking violation of cluster decomposition properties of the de Sitter invariant vacuum state”. It has also been shown that this growing of the graviton two-point function render scattering amplitudes divergent [13]. As a consequence, the authors of [13], among many others, suspect a quantum instability of de Sitter space, meaning that the de Sitter geometry is not a stable ground state of quantum gravity with a cosmological constant.

Other workers in the field, mainly motivated by the fact that the correlations of some gauge invariant quantities fall-off in the IR limit, claim that the non-vanishing of the two-point functions in the IR is nothing but a gauge artifact. For instance, the electromagnetic field correlation function is well-behaved in the IR [14] :

$$\langle F_{ab} F_{a'b'} \rangle = \frac{1}{8 \pi^2 R^2} \left( \frac{1}{1 - z} \right) \frac{1}{4} \left( g_{[a'[a} g_{b']b} + 4 n_{[a[a'} n_{b']b} \right).$$

The same is true for the graviton field as there is no growing terms in the correlation function of the Riemann tensor $\langle R_{ab;cd}(x) R_{a'b';d'}(x') \rangle$.

In the following we will study in detail the IR problem in the case of the photon field in de Sitter. The IR behavior of this field received considerably less attention in the literature than its counterpart for the mmc and the graviton fields. The correlation functions of these fields exhibit even stronger pathologies than the MMC scalar and the graviton fields. The correlation functions render scattering amplitudes divergent [15]. As a consequence, the authors of [15] among many others, suspect a quantum instability of de Sitter space - of quantum gravity with a cosmological constant. It led some authors [12] to speak of a “striking violation of cluster decomposition properties of the de Sitter invariant vacuum state”. It has also been shown that this growing of the graviton two-point function render scattering amplitudes divergent [13]. As a consequence, the authors of [13], among many others, suspect a quantum instability of de Sitter space, meaning that the de Sitter geometry is not a stable ground state of quantum gravity with a cosmological constant.

The equation of motion (3) applied to the two-point function

$$W_{aa'}^{[\lambda]}(x_1, x_2) = \alpha_1^{[\lambda]}(z) g_{aa'} + \alpha_2^{[\lambda]}(z) n_a n_{a'}.$$  \hspace{1cm} (6)$$

leads after some algebra to a coupled system of differential equations. Hereafter we will only need one of these equations, namely:

$$H \left[ 1 + \frac{1}{2} \frac{\lambda - \frac{1}{2}}{\lambda_{d} - 1} \right] \alpha_1 + \frac{\lambda - \frac{1}{2}}{\lambda_{d} - 1} \alpha_2$$

$$+ \frac{\lambda - \lambda_{d}}{\lambda_{d} - 1} \left[ \frac{1}{2} \frac{1}{1 - z} \right] \alpha_2 = 0$$  \hspace{1cm} (8)$$

where the prime denote derivation with respect to the
variable $z$, $\lambda_d = \frac{d - 3}{d - 1}$ and $H$ is the hypergeometric operator defined by

$$H[a, b, c] = z(1 - z) \frac{d}{dz} + \left[ c - (a + b + 1) \right] z \frac{d}{dz} - ab$$

Another, moreover first order, relation between $\alpha_1$ and $\alpha_2$ is obtained by considering the two-point function of the field strength

$$\langle F_{ab} F^{a'b'} \rangle = \beta_1 \left( g_{[a} g_{b]}^{a'} g_{b']} + \beta_2 n_{[a} g_{b]}^{a'} n_{b']} \right).$$

In fact, the equation of motion (in vacuum) $\nabla^a F_{ab} = 0$ implies the relation \[ (1) \]

$$\alpha_2 = \frac{z}{8\pi^2 R^2(z - 1)} + 2(1 - z) (z\alpha_1 + \alpha_1) \quad (9)$$

We now specialize our results to the $d = 4$ case for simplicity. The general solution in the Euclidean vacuum is found to be

$$\alpha_{1}^{[\lambda]}(z) = \frac{1}{48\pi^2 R^2 \lambda} \left[ \frac{3(\lambda + 1)}{2(1 - z)} + \frac{3\lambda - 1}{2z} + \left(3\lambda - 1\right) \left( \frac{1}{2z} + \frac{1}{2z^2} \right) \ln(1 - z) \right]$$

$$\alpha_{2}^{[\lambda]}(z) = \frac{1}{24\pi^2 R^2 \lambda} \left[ 1 - \frac{3(\lambda - 1)}{2(1 - z)} - \frac{3\lambda - 1}{2z} + 3(\lambda - 1) \left( \frac{1}{2z} + \frac{1}{2z^2} \right) \ln(1 - z) \right]$$

and the IR behavior is given by

$$\lim_{z \to 1} W_{a' a}^{[\lambda]}(x, x') = \frac{1}{24\pi^2 R^2 \lambda} n_{a} n_{a'}.$$

This result means that one can cure any IR bad behavior by going to the Landau gauge $\lambda \to \infty$. More importantly, we see that the IR behavior of the correlation function is pure gauge, thus asking whether or not the two-point function is well or ill-behaved in the IR is in itself -at least partially-a misleading question.

Finally we note that there exists a special choice of the gauge fixing parameter, namely $\lambda = \frac{1}{2}$ (more generally $\lambda_d$ in $d$ dimensions), that cancels logarithmic terms and gives a particularly simple two-point function. We note, perhaps as a curiosity for the time being, that for large dimensions $d$, $\lambda_d$ goes to the Feynman gauge $\lambda = 1$, which is the simplest gauge in flat space.

MORE PATHOLOGICAL GAUGES

We now consider a larger family of gauge fixing terms. Our motivation is that the IR pathology we exhibited in the last section, namely that the correlation function tends to a constant, might seem -I believe mistakenly mild enough not to worry about. We will show that in this more general gauge, the two-point function is actually growing in the IR, exactly like the mc scalar or the graviton fields. We consider the action

$$S_{\lambda, \xi} = S_{\lambda} + \frac{\xi}{2m^2} \int d^4x \sqrt{-g} \left( \nabla_a A^a \right) \left( \nabla_a A^b \right)$$

where we have added a higher derivative gauge fixing term. Similar higher derivative gauge fixing are occasionally used in QCD and the electro-weak theories. They were also used to study flat space perturbative quantum gravity. We note that if we want $\lambda$ and $\xi$ to be dimensionless, such higher derivative gauge fixing terms require the introduction of a mass quantity $m$. In flat space $m$ is introduced by hand, while in de Sitter space the inverse of the de Sitter radius plays naturally this role: $m^2 = \frac{\alpha}{R^2}$. This observation renders the introduction of higher derivative gauge fixing somehow more natural in the de Sitter case. The equation of motion reads

$$\left[ \Box_{ab} + (\lambda - 1) \nabla_a \nabla_b + \frac{\xi}{m^2} \Box_{a} \nabla_b \right] A^b = 0 \quad (12)$$

Flat space. The flat space Feynman propagator is found in Fourier space to be

$$\tilde{G}^F_{a'a'}(k) = \frac{g_{a'a'}}{k^2 - i\epsilon} + \frac{1 - \lambda}{\lambda (k^2 - i\epsilon)^2} + \frac{\xi}{m^2 \lambda^2} \left( \frac{1}{k^2 - i\epsilon} - \frac{1}{k^2 - \frac{\alpha^2}{\lambda^2} - i\epsilon} \right) k_a k_{a'}.$$

The reader will note the relative negative sign typical of higher derivative theories in front of the last propagator. Using \[ (1) \] and its derivatives the coordinate-space two-point function is then found to be

$$W_{a'a'} = \left[ 1 - \frac{1}{2\pi^2 m^2 \lambda^4 \mu^2} + \frac{1}{\pi^2 m^2 \lambda^4 \mu^2} + \frac{K_2(\imath m \nu)}{4\pi^2 \lambda^2 \mu^2} \right] g_{a'a'} + \left[ \frac{2}{\pi^2 m^2 \lambda^4 \mu^2} + \frac{1 - \lambda}{4\pi^2 \lambda^2 \mu^2} + \frac{K_0(\imath m \nu)}{4\mu^2} \right] n_{a} n_{a'} + i \left( \frac{\mu^2}{4\pi^2 \lambda^2 \mu^2} - \frac{2}{\pi^2 m^2 \lambda^4 \nu} \right) K_1(\imath m \nu) n_{a} n_{a'}$$

where we have introduced the quantity $\nu = (\lambda/\xi)^{1/2}$. For all values of $\lambda$ and $\nu$, this expression vanishes for large timelike and spacelike separations as expected. The short distance singularity is given by

$$W_{a'a'} \sim \frac{1}{8\pi^2 \mu^2} (g_{a'a'} - 2n_{a} n_{a'}).$$

We emphasize that the short distance singularity of the two theories \[ (1) \] and \[ (11) \] are different. This is due to the non commutation of the limits $\xi \to 0$ and $\mu \to 0$.

De Sitter space. We now consider the action \[ (11) \] in de Sitter space and thus set $1/m^2 = R^2$. Following the same methods described above we obtain the following
equations on \( \alpha_1 \):
\[
\alpha_1^{(4)} = \frac{4(t - 2)(t + 3)}{(t - 1)^2z^2} \alpha_1 + \frac{3(z - 1)}{(t - 1)^2z^2} \alpha_1^{(2)},
\]
\[
-12 - (z - 1)(z + 3) \alpha_1^{(3)} + 8 \left( \frac{1}{z + 1} \right) \alpha_1^{(2)}
\]
where we introduced the parameter \( \tau = \frac{\sqrt{1 - z}}{2\sqrt{z}} \). Obtaining this equation requires some elaborated algebraic manipulations. The calculations in this section were thus verified with the tensor algebra system xAct on Mathematica [1]. This equation can be solved in closed form. Using the asymptotic formulas in table [2] the solution verifying: i) regularity at \( z = 0 \) and ii) flat space short distance singularity is found. For non integer values of \( \tau \) it reads
\[
\alpha_1^{[\lambda, \tau]}(z) = \frac{2Q_2^2(2z - 1) - \pi \cot(\pi \tau)P_2^2(2z - 1)}{32\pi^2 R^2 \lambda (z - 1)(\tau^2 + \tau - 2)} + \frac{3}{96\pi^2 R^2 \lambda \left( (2z - 1)(1 - z) + 1 \right)}
\]
\[
+ \frac{1}{32\pi^2 R^2 \lambda \left( (\lambda - 1)(\tau + 1) - 2\lambda \right)} \left( \frac{\lambda + 1}{z - 1} \right) \frac{1}{z - 1} \frac{\lambda + 1}{\tau + 1 - 2\lambda}
\]
where \( P \) and \( Q \) are Legendre functions of the first and second kind respectively. As before, \( \alpha_1^{[\lambda, \tau]} \) is obtained by [3]. The asymptotic behavior in the IR is given by \( \tau > 1 \):
\[
\alpha_1^{[\lambda, \tau]}(z) \sim \frac{2^{\tau - 5} \cot(\pi \tau) \Gamma \left( \tau + \frac{1}{2} \right)}{\pi^3/2^2 R^2 \lambda (\tau + 2) \Gamma(\tau)} z^{-\tau - 2}
\]
\[
\alpha_2^{[\lambda, \tau]}(z) \sim \frac{2^{\tau - 1}(\tau - 1) \tau \cot(\pi \tau) \Gamma \left( \tau + \frac{1}{2} \right) \Gamma \left( \tau + \frac{3}{2} \right)}{\pi^3 R^2 \lambda (2\tau + 3)(2\tau^2 + 5\tau + 2) \Gamma(\tau + 2)} z^{-\tau - 1}
\]
Thus for \( \tau > 2 \) for instance, the two-point function grows like \( z^{-\tau - 2} \) in the IR. This strong IR growing is purely a gauge artifact since, as proven in the beginning of this letter, no IR pathologies arise in the Landau gauge.

\[
\begin{array}{c|c|c|c}
\alpha_1^{(2)}(2z - 1) & z \to 0 & z \to 1 & z \to \infty \\
\hline
p_2^{(2)}(2z - 1) & -\frac{\sin(\pi \tau)}{\pi z} \Gamma(\tau + 3) \left( \frac{3}{\tau \Gamma(\tau - 1)} \right) (z - 1) & \frac{2^{\tau - 1} \Gamma(\tau + 3/2)}{\sqrt{\pi} \Gamma(\tau - 1)} z^{\tau - 2} & \frac{2^{\tau - 3} \Gamma(\tau + 3/2)}{\sqrt{\pi} \Gamma(\tau - 1)} z^{\tau - 1}
\end{array}
\]

\[
\begin{array}{c|c|c|c}
\alpha_1^{(3)}(2z - 1) & z \to 0 & z \to 1 & z \to \infty \\
\hline
Q_2^{(2)}(2z - 1) & -\frac{\cos(\pi \tau)}{2z} \frac{1}{(z - 1)} & \frac{1}{2} \Gamma(\tau + 3) & \frac{1}{2} \Gamma(\tau + 3) \frac{1}{z^{\tau - 1}}
\end{array}
\]

### Table 1. Asymptotics of the Legendre functions near singular points.

### A PHYSICAL DECOMPOSITION

The previously described situation, namely that the IR behavior of the two-point function in de Sitter space contains important gauge artifacts makes it natural to look for a decomposition of the two-point function into a physical and a non-physical parts. We show now that such a decomposition exists and is given by the following rewriting of the two-point function
\[
W_{\text{IR}}^{[\lambda]}(x, x') = g_{aa'} \beta_1(z) + \nabla_a \nabla_{a'} \beta_2(z).
\]
In fact, most of the physics is included in the “quantum” action \( W_J \) defined by
\[
\exp \left[ \frac{i}{\hbar} W_J \right] = \int D[A_{a}] \exp \left[ \frac{i}{\hbar} S + \int d^4 x \sqrt{-g} A_{a} J^a \right]
\]
where \( J_a \) is an external conserved current \( \nabla_a J^a = 0 \). The tree-level expression of the effective action is given by
\[
W_J = \int dV_x dV_{x'} J^a(x) W_{\text{IR}}^{[\lambda]}(x, x') J^{a'}(x')
\]
differential \( dV_x \) is the invariant volume element. Since the current \( J_a \) is conserved, integration by parts ensures that only \( \beta_1 \) will contribute to \( W_J \) and it thus sufficiently be referred to as the “physical” two-point function. An explicit form of the functions \( \beta_1 \) and \( \beta_2 \) can be found by solving the system
\[
\alpha_1 = \beta_1 + \frac{1}{2R^2 z^2} \beta_2, \quad R^2 \alpha_2 = (1 - z) \beta_2 + z(1 - z) \beta_2'.
\]
The solutions are unique if one requires regularity near \( z = 0 \) and we obtain

\[
W_{\text{IR}}^{[\lambda, \tau]}(x, x') = -\frac{1}{16\pi^2 R^2} \left( \frac{1}{1 - z} + \frac{\ln(1 - z)}{z} \right) g_{aa'}
\]

It is a remarkable (and expected) fact that \( W_{\text{IR}}^{[\lambda, \tau]} \) independent and is well behaved in the IR. In flat spacetime, the Feynman gauge \( (\lambda = 1, \xi = 0) \) gives precisely this physical two-point function. The situation in de Sitter is quite different and no choice of the gauge fixing parameters gives the physical two-point function. A natural question is whether a more general gauge fixing term gives directly \( W_{\text{IR}}^{[\lambda, \tau]}(x, x') \) in de Sitter space.

**OUTLOOK**

We showed that the IR pathological behavior of the photon's two-point function is nothing but a gauge artifact. We suggest that the situation is similar for the graviton field. The IR behavior of the latter is however necessarily more intricate since it has been shown that the (transverse-traceless) growing term of the two-point function does not cancel out from scattering amplitudes [4]. This implies in particular that a decomposition like [4] does not lead to a well-behaved “physical” two-point function. The IR behavior of the graviton field will be examined in [2].
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