Comparing Models for IMF Variation Across Cosmological Time in Milky Way-like Galaxies

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To be submitted to MNRAS, 19 July 2017

ABSTRACT

One of the key observations regarding the stellar initial mass function (IMF) is its near-universality in the Milky Way (MW), which provides a powerful way to constrain different star formation models that predict the IMF. However, those models are almost universally “cloud-scale” or smaller — they take as input or simulate single molecular clouds (GMCs), clumps, or cores, and predict the resulting IMF as a function of the cloud properties. Without a model for the progenitor properties of all clouds which formed the stars at different locations in the MW (including ancient stellar populations formed in high-redshift, likely gas-rich dwarf progenitor galaxies that looked little like the Galaxy today), the predictions cannot be fully explored, nor safely applied to “live” cosmological calculations of the IMF in different galaxies at different cosmological times. We therefore combine a suite of high-resolution cosmological simulations (from the Feedback In Realistic Environments project), which form MW-like galaxies with reasonable star formation properties and explicitly resolve massive GMCs, with various proposed cloud-scale IMF models. We apply the models independently to every star particle formed in the simulations to synthesize the predicted IMF in the present-day galaxy. We explore models where the IMF depends on Jeans mass, sonic or “turbulent Bonner-Ebert” mass, fragmentation with a polytropic equation-of-state, or where it is self-regulated by protostellar feedback. We show that all of these models, except the feedback-regulated ones, predict far more variation (∼ 0.6 – 1 dex 1σ scatter in the IMF turnover mass) in the simulations than is observed in the MW.

Key words: stars: formation – turbulence – galaxies: star formation – cosmology: theory

1 INTRODUCTION

The (instantaneous) mass distribution of stars at their formation time, also known as the initial mass function (IMF), is one of the key predictions of any star formation model. This governs essentially all observable and theoretical aspects of star formation and stellar populations – observable luminosities and colours; effects on stellar environments via feedback in the form of stellar winds, radiation, supernovae; nucleosynthesis and galactic chemical evolution, and so on. The IMF has been well-studied within the MW, and appears to be well-fit by a simple function with a Salpeter (1955) power-law slope at high masses and lognormal-like turnover at low masses (Chabrier 2005; Kroupa 2002). Perhaps the most interesting feature of the IMF is its universality: it has been found that there is quite weak variation within the MW (for recent reviews, see Chabrier 2003; Bastian et al. 2010; Offner et al. 2014; Krumholz 2014, and references therein), albeit with a few possible outliers (e.g. Luhman et al. 2009; Kraus et al. 2017). As Offner et al. (2014) emphasize, this universality includes both very young (∼ Myr-old) and very old (∼ 10 Gyr-old) stellar populations; stars forming in small, nearby GMCs with masses ∼ $10^2 – 10^5 M_\odot$ and massive complexes with masses ∼ $10^5 – 10^6 M_\odot$; the solar neighbourhood at ∼ 10 kpc from the galactic centre (where the gas disk surface density is ∼ $10 M_\odot$ pc$^{-2}$) and the central molecular zone at sub-kpc and ∼ 100 pc scales (where gas surface densities are order-of-magnitude larger).

In other galaxies, the IMF usually must be assumed, and with an IMF assumption, physical properties of the stellar populations and galaxies (e.g. their stellar masses) are derived from observables (e.g. light, colours). This makes it critical to understand the IMF, in order to understand galaxy formation. Likewise it is critical for models of galaxy formation to predict or assume some IMF model, in order to make any meaningful predictions for observable quantities. The universality of the IMF in old stellar populations in the MW is widely taken as a suggestion that it may be near-universal in other galaxies, because older populations in the MW formed when the galaxy was much younger and very different, likely a typical high-redshift gas-rich, metal-poor dwarf galaxy. There are indirect constraints on the IMF both from spectral features and integrated mass-to-light constraints in nearby galaxies; these mostly also favor a universal IMF (e.g. Fumagalli et al. 2011; Koda et al. 2012; Andrews et al. 2013, 2014; Weisz et al. 2015). More recently there have been more interesting hints of variation in the centres of massive elliptical galaxies (van Dokkum & Conroy 2010, 2011; Conroy & van Dokkum 2012; Treu et al. 2010; Sonnenfeld et al. 2015; Cappellari et al. 2012; Posacki et al. 2015; Martín-Navarro et al. 2015b,a,c), and perhaps also in faint dwarf galaxies (Overstien & Glazebrook 2008; Brown et al. 2012; Geha et al. 2013). Even so, it is worth stressing that the implied variation is not radical: it implies variation of a factor < 2 in the stellar mass-to-light ratio.
As a result, there is a long history of both theoretical and empirical models for galaxy formation which have attempted to predict the IMFs that should arise in different galaxy populations, as a function of either galaxy-scale or \( \sim \)kpc-scale properties (what can be resolved in most previous calculations) within the galaxies (see e.g. Baugh et al. 2005; van Dokkum 2008; Hopkins 2013; Davé et al. 2012; Narayanan & Davé 2012; Recchi & Kroupa 2015; Lacey et al. 2016; Blanchac et al. 2016). At the same time, the specific hints of galaxy-to-galaxy variation discussed above have prompted a new wave of theoretical models which argue the IMF could vary under certain conditions at the GMC or sub-GMC scale, in a way that may connect to the systematic variation inferred in different galaxies (e.g. Weidner et al. 2013; Bekki 2013; Chabrier et al. 2014; Ferreras et al. 2015).

However, these models in every case rely on very strong simplifying assumptions – the IMF is predicted as a function of the cloud properties out of which the stars form, such as its temperature, density, turbulent velocity dispersion, virial parameter, etc. (from which properties like the Jeans mass, or the turbulent Bonner-Ebert mass, or the IGIMF turnover mass, are determined). It is impossible at present to know these empirically because all the clouds that formed the old stellar populations in a galaxy (or even for most clouds within a galaxy at present day), so instead some strong additional assumptions are usually applied. For example, authors assume isothermal gas with \( T = 10^4 \text{K} \) (or some other temperature) at all densities, a universal linewidth-size relation across all galaxies, redshifts, and regions within galaxies, or a Jeans or sonic mass within clouds that somehow scales proportionally to that measured from the gas at the \( 2 \text{kpc} \) scales resolved in the cosmological calculations. But if these properties vary across cosmic time, or cloud-to-cloud, then any such model will produce variation in the predicted IMF which can be compared to the observational limits within the MW.

In this paper we therefore investigate the predicted variation in the IMF peak imprinted by these physics in a number of IMF models. We combine high-resolution simulations of MW-like galaxies (where the cloud-scale properties can be at least partially resolved) with the relevant small-scale models for IMF variation as a function of cloud properties.

## 2 Model and Methodology

### 2.1 Simulation

We utilize a set of numerical simulations of MW-like galaxies (see Table 1) presented in Hopkins et al. (2017), from the Feedback in Realistic Environments (FIRE) project (Hopkins et al. 2014).\(^1\) The simulations are fully cosmological “zoom-in” simulations (where resolution is concentrated on one galaxy in a large cosmological box, run from redshift \( z > 100 \) to today) and are run using GIZMO (Hopkins 2015)\(^2\), with the mesh-free Godunov “MFM” method for the hydrodynamics (Hopkins 2015). Self-gravity is included with fully-adaptive force and hydrodynamic resolution; the simulation mass resolution is fixed at 7000 or \( 56000 \ M_{\odot} \).

\(^1\) http://fire.northwestern.edu

\(^2\) http://www.tapir.caltech.edu/~phopkins/Site/GIZMO.html

![Figure 1. Visualization of the starlight (mock ugr composite image, accounting for each stellar sink-particle’s age and metallicity and ray-tracing including dust obscuration) from one of the simulated MW-like galaxies (see Table 1) we use in our calculations (galaxy m12i from Hopkins et al. 2017 with 56000, \( M_{\odot} \) resolution). Note that resolved molecular clouds and arms are evident. See Fig. 2 for the other galaxies from Table 1.](http://www.tapir.caltech.edu/~phopkins/Site/GIZMO.html)
in § 1) adopt a dynamical IMF model based on resolution-scale properties. But it has not been asked whether the models they considered violate observational constraints in the MW. (2) Stars at a given present-day position in a galaxy can form at wildly different times/places (some even in other dwarf galaxies). This is especially true for the stars in old MW clusters, which appear to have formed at high redshifts, probably in distinct dwarf galaxies with entirely distinct radiation fields, turbulent velocity dispersions, gas masses, etc. It is impossible to know the distribution of progenitor cloud properties at star formation for old stars (needed for a given IMF model to make predictions) from observations (or localized simulations) alone.

The galaxies studied here, shown in Figs. 1–2 – have been studied extensively in previous work: they are similar to the MW in their stellar mass, present-day gas fractions and SFRs (Hopkins et al. 2014), and metallicity (Ma et al. 2016b). Our “fiducial case” m12i is also similar to the MW in its stellar kinematics, thin-thick disk morphology, metallicity gradient and metal abundance ratio gradients (in both vertical and radial directions) stellar age distribution (Ma et al. 2016a, 2017), R-process element distribution (van de Voort et al. 2015) and galactic stellar halo and satellite dwarf population (Wetzel et al. 2016). The other two examples represent a slightly later-type (m12f) and earlier-type (m12m) galaxy, at the same stellar mass and SFR. This is particularly useful because of course no simulation will exactly match the formation history of the MW, so it is important to understand whether our predictions are sensitive to this.

These and other FIRE simulations have also been shown to reproduce the observed Kennicutt-Schmidt relation (Sparre et al. 2015; Orr et al. 2017), properties of galactic outflows (Muratov et al. 2015) and (in higher resolution, non-cosmological simulations) the observed mass function (and CO luminosities), size-mass, and linewidth-size distributions of GMCs (Hopkins et al. 2012, 2013). One might reasonably worry that this cannot be captured at the lower resolution necessary in cosmological simulations. Therefore in Fig. 4 we plot the mass function and linewidth-size relation of GMCs identified at present-day in the actual simulations studied here. They appear to agree at least plausibly with observed properties (Dobbs et al. 2014; Heyer & Dame 2015). Note that our mass resolution introduces a cutoff at the low mass end of the GMC mass function because these clouds can not be resolved by the simulation. However, all simulations included in this paper do resolve the most massive GMCs (> 10^6 M☉), in which most of the mass is con-

Figure 2. Face on (top) and edge on (bottom) visualizations of starlight (mock ugr composite image, accounting for each stellar sink-particle’s age and metallicity and ray-tracing including dust obscuration) for the simulated MW-like galaxies from Table 1. Unlike Fig. 1 the m12i example shown here is from the high resolution (7000 M⊙) run. The MHD run is not shown as it gives virtually identical results as the non-MHD runs (see Su et al. 2016). Note the edge-on images of m12i and m12f are a mock Galactic (Aitoff) projection from a random star at ∼ 10 kpc from the galactic center. For more details on the individual runs see Hopkins et al. 2017.
models we investigate). Specifically, whenever a sink particle is spawned, we record all properties of the parent gas element from which it formed, and use these in post-processing to predict the IMF. Fig. 5 shows the properties of gas elements at one instant, $z = 0$, weighted by star formation rate. Integrating over all times and all galaxies which form stars that ultimately reside in the final galaxy, Fig 6 shows the density and temperature distribution of these “star forming particles” (gas at the moment the simulation assigned its mass to a sink particle) at the time of their formation, from our high-resolution m12f run. Not surprisingly most sinks form around the simulation density threshold from this particular run ($\sim 1000 \text{ cm}^{-3}$). This choice has no effect on the scatter in both $\rho_{\text{cloud}}$ and $T_{\text{cloud}}$, which are the relevant parts to our study. Scatter in these quantities translate to a scatter in the local IMF according to the IMF models we are studying. Note that Narayanan & Hopkins (2013) show the inferred temperature range from mock CO-ladder observations will tend to be significantly smaller than the range plotted here. We wish to emphasize that what is plotted in Fig. 6 is not the density/temperature of the core or proto-stellar gas that directly collapses and forms stars; that is not resolved in these simulations. Instead these are the properties of the progenitor molecular clouds, measured at the smallest resolved scales, which will (and must, physically) fragment into denser sub-clumps that can directly form stars. Also, the width in this distribution is expected to be higher than in present day clouds because of the longer lifetime of stars which preserves the progenitor cloud properties in their IMF for cosmological timescales.

2.2 From Parent Cloud to IMF Properties

From this point we infer the IMF turnover mass from the initial conditions of these parent clouds. This exercise has been done in detail by Guszejnov et al. (2016) where the semi-analytical framework of Guszejnov & Hopkins (2016) was utilized to create a mapping between GMC properties and the IMF. Fig. 7 shows how the IMF peak scales with initial temperature in an equation of state (EOS) and a protostellar feedback based IMF model. Such scaling relations can be analytically derived for other IMF models (e.g. Jeans mass) as well – we focus here on how each model predicts the turnover or “critical” mass $M_{\text{crit}}$ scale, because this is the most identifiable feature of the IMF (it sets the mass-to-light ratio, and varies significantly between models). In contrast the bright-end slope varies negligibly between models, so it is not useful as a diagnostic.

In this paper we investigate the sensitivity to initial conditions for the following classes of IMF models (summarized in Table 1):

- Jeans mass models: The Jeans instability is the primary mechanism for the collapse of gas clouds into stars,

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**Figure 4.** Top: Mass function (MF) of GMCs in the fiducial simulation (Fig. 1) at \( z = 0 \), at different mass resolution (baryonic particle mass \( m_i = 1000 m_{\text{HH}} M_\odot \)). We restart the fiducial simulation from Fig. 1 (with \( m_i = 1000 M_\odot \)) at \( z = 0.1 \), after re-sampling the particles to raise/lower the mass resolution. We then evolve it for \( \sim 1 \) Gyr to \( z = 0 \), and measure the MF of dense cold-gas clouds (identified in post-processing with a friends-of-friends group-finder) time-averaged over the last \( \sim 100 \) Myr inside \( < 20 \) kpc of the galaxy center. All details of the resampling and group-finding method are in Hopkins et al. (2017). We compare the observed MW GMC MF from Rice et al. (2016), normalized to the same total mass, measured inside (solid) and outside (dotted) the solar circle. At all resolutions, a GMC MF similar to that observed is recovered. The most massive GMCs contain most of the mass/star formation and are the first-resolved. At higher resolution we extend to smaller GMCs. Bottom: Linewidth-size relation for the same clouds (median in thick lines; 5–95% intervals in thin lines), vs. observations in nearby galaxies (Bolatto et al. 2008; Fukui et al. 2008; Heyer et al. 2009; Muraksa et al. 2009; Roman-Duval et al. 2010; Colombo et al. 2014; Heyer & Dame 2015; Tosaki et al. 2017); note our definition of \( R_{\text{cloud}} \) is equivalent to their \( \sigma_r \). The predicted normalization and 1 \( \sigma \) dispersion (\( = 0.12 \) dex, although it increases slightly to \( = 0.2 \) dex at the lowest masses) are consistent with observations (compare e.g. Kaufmann et al. 2013). There is no systematic resolution dependence (other than sampling smaller clouds at higher resolution).

**Figure 5.** Density-temperature diagram for gas at present-day (\( z = 0 \)) in our high-resolution m12i simulation (others are similar). Colors show a 2D histogram colored by the gas-mass per-pixel (log-weighted, increasing black-blue-green-red with a \( \sim 6 \) dex stretch), so this is peaked where there is significant mass in a narrow temperature range. HII regions, warm ionized medium, and warm and cool neutral phases are evident (we do not show lower densities where hot gas is prevalent). Solid (dashed) lines show the median (inter-quartile) temperature of all gas denser than \( > n \), weighted by mass (white) or star formation rate (red). The latter converges rapidly because SF is restricted to high-\( n \) gas. At \( z = 0 \) in the simulation, most SF occurs in gas with \( n > 1000 \) cm\(^{-3}\) and \( T \approx 50 \) K.

**Figure 6.** Density-temperature diagram (as Fig. 5; same galaxy), but for the progenitor clouds (gas elements which formed a stellar sink particle) of all stars which reside in the \( z = 0 \) galaxy (integrated over all cosmic time). Note these are the cloud properties at the moment the sink formed, weighted by mass in stars today (colors use \( \sim 3 \) dex stretch). As expected, most sinks form a factor of a few above our minimum threshold (\( n_{\text{crit}} = 1000 \) cm\(^{-3}\)), though some gas reaches much higher densities. Lines again show the median and inter-quartile range for stars formed at resolved densities \( > n \). Accounting for different times and progenitor galaxies, the dispersion in temperatures at a given density is a factor \( \sim 3\)–4 larger here than for star-forming gas just at \( z = 0 \).
these cases are: curs at a critical surface density \( \Sigma_c \). Motivated by radiation transfer simulations like Bate 1976; Whitworth et al. 1998; Larson 2005; Glover & \( \rho \) occur at a critical volume density \( \rho_c \) at the Jeans mass at this density. This can it becomes opaque to its own cooling radiation, leading to a fragmentation at the Jeans mass. This can be seen (taken to be that which encloses the nearest \( \sim 32 \) gas neighbours).

- **Protostellar feedback models**: Although there are a number of ways newly-formed stars can regulate star formation, most studies have concluded that at the scale of the IMF peak (early protostellar collapse of \( \sim 0.1 M_\odot \) clouds) the most important self-regulation mechanism is radiative feedback from protostellar accretion (Bate 2009; Krumholz 2011; Guszejnov et al. 2016). This sets a unique mass and spatial scale within which the protostellar heating has raised the temperature to make the core Jeans-stable, terminating fragmentation. The resulting critical masses are

\[
M_{\text{crit},S} = M_{\text{sonic}} \sim \frac{2 c_s^2 R_{\text{sonic}}}{G},
\]

where \( R_{\text{sonic}} \) is defined through the linewidth-size relation

\[
\sigma^2_{\text{turn}}(\lambda) = \frac{c_s^2}{R_{\text{sonic}}}. \tag{4}
\]

In our calculations \( \sigma_{\text{turn}} \) is estimated from the simulations when a star particle forms by measuring the velocity dispersion (after subtracting the mean shear) between neighboring particles in a sphere of radius \( \lambda \). The variation in the IMF predicted by some of the models can be significant, with different implementations of the same theory leading to different results.

3 RESULTS AND DISCUSSION

Fig. 8 shows that there is significant variation the properties of the progenitor GMC complexes which formed stars that ultimately end up at a specific galacto-centric radius. We stress that this is not the variation of properties in present-day star-forming clouds, but includes all variations in time as well: if the galaxy progenitor was gas-rich (gas fraction \( \sim 1/2 \)) at \( z \sim 1 - 2 \) for example, then the midplane gravitational pressure \( \sim G \Sigma_\text{gas}^2 \) would have been a factor \( \sim 100 \) larger than in the galaxy today. Fig. 9 shows that this, in turn, produces large IMF variations in all models here except those accounting for protostellar heating. Such variations are strongly ruled-out by observations (Bastian et al. 2010). Note that these results are robust to variations in simulation parameters (see Table 1).

The variations in the IMF predicted by some of the simple models here (e.g. the Jeans-mass models) have often been substantially underestimated in previous work in the literature. In analytic models of the IMF (see references in Sec. 1) or galaxy-scale models which fail to resolve individual “parent clouds”, but post-process the entire galaxy (with \( > \text{kpc-scale resolution} \)) to determine an IMF (Narayanan & Davé 2012; Hopkins 2013; Blancato et al. 2016), it is commonly assumed that all star-forming clouds are uniformly at
the same isothermal temperature (e.g. $T = 10$ K at all densities), virial parameter, and lie exactly on the same linewidth-size relation. For example, if the gas at all densities and all cosmic times had exactly the same temperature, then the variation in the IMF for the opacity-limited EOS models would vanish (all clouds and cores lie on exactly one adiabat). This assumption is not correct, however, as even in the present-day MW (e.g. fixed redshift and galaxy properties) both GMC and clump temperatures (e.g. Bergin & Tafalla 2007; Mills & Morris 2013; Sánchez-Monge et al. 2014; Ott

Table 1. Rows: Different IMF models compared in this paper, each with the predicted scaling of the IMF turnover mass $M_{\text{crit}}$ with initial parent cloud properties (§ 2.2), reference, and the predicted standard deviation in log($M_{\text{crit}}$) across the galaxy at present-day (averaging Fig. 8 over all galacto-centric radii). We measure $\sigma_{M_{\text{crit}}}$ from five simulations: galaxies $m12i$, $m12f$, and $m12m$ are three distinct Milky Way-mass ($\sim 10^{12} M_{\odot}$) halos which produce similar diskly, Milky Way-like galaxies (stellar mass $\sim 0.5 \times 10^{11} M_{\odot}$), but have different formation histories (see Fig. 2 for visualizations and Hopkins et al. 2017 for details). For each we label the mass resolution (in $M_{\odot}$) and minimum density $n_{\text{crit}}$ for creation of stellar sink particles. For $m12i$, we compare two alternative runs: one at lower resolution, and one including magnetic fields ($m12i+\text{MHD}$). The predicted IMF variation is remarkably robust across all these simulations.

Figure 8. Standard deviation in star-forming progenitor cloud properties (measured at the time of star formation, as in Fig. 6), across the progenitor clouds of all stellar sink particles which reside at a given present-day galacto-centric radius (in our fiducial $m12i$ run with $56000 M_{\odot}$ resolution; however the dependence on radius is weak and all our simulations in Table 1 give similar results). Note that this is not the variation of present-day star forming clouds at different radii, as stars at some present-day radius could have formed at wildly different times and positions (for example, at high redshift in a more gas-rich disk with much larger pressures and densities). Thermodynamic and turbulent progenitor-cloud properties vary by $\sim 0.3-0.5$ dex; this implies large IMF variations for any model which has a strong dependence on these quantities.

Figure 9. Mean (top) and standard deviation (bottom) of the IMF turnover mass $M_{\text{crit}}$ normalized its galactic average ($\langle M_{\text{crit}} \rangle$) at different galacto-centric radii (in our fiducial $m12i$ run with $56000 M_{\odot}$ resolution). We compare the IMF models in Table 1 and the observationally allowed range of scatter in the IMF across the Milky Way, from Bastian et al. (2010). In these simulations, only models accounting for protostellar heating avoid strongly overpredicting the scatter in MW IMFs. The models are shown here for the same galaxy in Fig. 8, but we obtain very similar results for each of the five simulated galaxies in Table 1.
et al. 2014; Nishimura et al. 2015)\(^4\) and virial parameters (e.g. Kauffmann et al. 2013; Svboda et al. 2016) vary substantially. As expected variations are more pronounced in other nearby dwarf or star-forming galaxies (Gorski et al. 2017; Tang et al. 2017) or redshift \(z \gtrsim 1\) − 2 galaxies and starburst systems (see e.g. Ott et al. 2011; González-Alfonso et al. 2012; Narayan & Krumholz 2014; Mangum et al. 2013; Miyamoto et al. 2015; Zschaechner et al. 2016), which are better analogues to the progenitors where many of the stars in the present-day Galaxy formed.

It is certainly possible that we (and these observations) have over-estimated the range of temperatures of GMCs in different environments. But the strong temperature sensitivity of the EOS models (e.g. \(\alpha T^2\)) means that the temperature of all progenitor clouds, at all redshifts and in all progenitor galaxies, which formed stars in today’s MW, would have to lie within a scatter of just \(\sim 20\%\) in temperature (smaller than that observed in just solar-neighbourhood clouds) in order to avoid exceeding the allowed IMF variation in the MW.

Moreover the linewidth-size relation is observed to vary systematically, both within the MW and galaxy-to-galaxy, with high-redshift galaxies (the progenitors of the MW) differing by more than an order of magnitude (see e.g. Swinbank et al. 2011, 2015; Canameras et al. 2017, and references therein). Even if temperature variations are neglected entirely, in the “Turbulent/Sonic Mass” models the turnover mass is proportional to the square of the deviation \((\sigma_{\text{cloud}}/\rho(\gamma))\) of each cloud from the linewidth-size relation (Hopkins 2012; Hennebelle & Chabrier 2008), but these deviations are observed to be \(\sim 0.3\) − 0.5 dex even within the MW at present-time (Bolatto et al. 2008) implying \(> 0.6\) dex scatter. Likewise the density dependence in “Jeans Mass” models predicts \(> 0.3\) dex scatter even if all temperature variations, time variations, and progenitor-galaxy variations are neglected (e.g. if we use only the scatter in cloud densities observed in the solar neighborhood of the MW at the present instant).

Recall, the cloud properties we use to predict the IMF are measured at a density scale of \(\sim 1000\) cm\(^{-3}\) and mass scale \(\sim 7000\) − 56000 M\(_\odot\). Obviously the clouds must continue to evolve and fragment to form actual stars – this is what our cloud-scale IMF models attempt to model. One might wonder, however, whether during this process some of the scatter might be reduced (if, for example, the clouds all converged to the same temperature eventually, owing to some additional physics). In the opacity-limited models, the equation of state (EOS) is specified (generally the cloud cools with \(T \propto \rho^{0.3}\)) to some density, becomes approximately isothermal, then becomes adiabatic above the opacity-limit density), so this is already built into the model explicitly. In the “Jeans Mass” or “Turbulent/Sonic Mass” models, we have implicitly assumed an isothermal EOS within each cloud so their temperature was assumed to be constant throughout their evolution and set by the initial conditions. One might, therefore, consider a more complicated version of these models (different from the simple scalings used thus far). Let us assume star formation occurs above some critical density \(\rho_{\text{crit}}\) and the gas follows a polytropic EOS with index \(\gamma\). The critical mass (Table 1) will then depend on \(M_{\text{crit}}(\rho_{\text{crit}}) = T_{\text{crit}}(\rho_{\text{crit}}/\rho_{\text{cloud}})^{-1}\), as \(M_{\text{crit}} \propto T_{\text{crit}}^{\alpha}\), where \(\alpha = 3/2, 1\) for the Jeans and Turbulent/Sonic models, respectively. Some simple algebra then gives us logarithmic variations in \(M_{\text{crit}}\), \(S_{\log M_{\text{crit}}} = \alpha S_{\log T_{\text{cloud}}} + [\gamma - 1] S_{\log \rho_{\text{cloud}}}\). Putting in the actual values (Fig. 8) this gives a dispersion \(\sigma_{\log M_{\text{crit}}} = 0.6, 0.4\) dex for the Jeans and Turbulent/Sonic models (for any \(\gamma \sim 0.5\) − 1.5). This reduces the predicted IMF variation, but still leaves it far larger than observed.

Thus we have shown that some additional physics on cloud or sub-cloud scales must be accounted for to reconcile the predictions of the “no-feedback” IMF models with the (weak) IMF variations observed in the MW. The “protostellar heating” models represent one physically-motivated class of models that do exactly this. Of course there may be others, but, broadly-speaking, they would need to either (a) strongly reduce the level of dependence of the predicted IMF on cloud properties (as the protostellar heating models do), or (b) strongly reduce the variation in GMC-scale properties predicted across cosmic time in the progenitor galaxies that form the MW. The latter is not impossible but seems to contradict the direct observations cited above, showing large variations in cloud properties in distant galaxies.

3.1 Caveats

Of course detailed, complex simulations (like the cosmological FIRE runs we are using) employ a large number of approximations to make problems numerically tractable. Although these simulations have been extensively vetted numerically (for details see Hopkins et al. 2017) some caveats worth noting include:

- Our analysis uses a somewhat arbitrary \(\rho_{\text{crit}} = 1000\) cm\(^{-3}\) minimum density threshold for star formation, based on numerical considerations. Using a much higher threshold would require much greater mass resolution (or else it would introduce severe numerical artifacts), which is not computationally feasible (these are the highest-resolution cosmological simulations of MW-mass galaxies ever run, at present). However, within the range we can probe, our results do not appear to depend sensitively on the density threshold or other numerical criteria for star formation.\(^5\)

- In the simulations, gas elements are replaced by star particles instantaneously once all star formation criteria and timescales are satisfied, so star formation happens in

\(^4\) Note that Nishimura et al. (2015) only focuses on Orion A and B so these results are not necessarily representative of the entire MW. Also, as our stars form primarily around \(\rho_{\text{crit}} = 1000\) cm\(^{-3}\), the average temperature of the progenitor clouds is higher than the observed GMCs because they have not reached the cooler, higher-density fully-molecular phases (see Figs. 5-6).

\(^5\) In Orr et al. (2017), we show the results of a number of simulations where we re-run our m12i galaxy from \(z = 0.1\) – 0.0, as in Fig. 4, but vary the numerical SF criteria. This includes changing the minimum SF density (from \(\sim 10 \sim 1000\) cm\(^{-3}\)), removing requirements that the gas be molecular and/or self-gravitating, and changing the efficiency per free-fall time with which gas that meets this criteria will turn into stars (from \(\sim 1\%\)). We have re-run our analysis, restricted to just those stars formed over the period the simulations were re-run, and find these changes do not significantly influence the predicted IMF variations.
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4 CONCLUSIONS

In this paper we explore the application of broad classes of IMF models to high-resolution fully-cosmological galaxy formation simulations. Stars at a present-day location might have formed at very different times and places, in an environment radically different from today's MW: only by using a cosmological simulation instead of local simulations or observations can we predict the properties of their progenitor star-forming clouds at these times and places, and therefore use these models to predict e.g. IMF shape variations, the predicted IMF in different sub-regions of the galaxy (e.g. the galactic nucleus), and the IMF in specific populations (e.g. metal-poor globular clusters versus present-day stellar populations).

ACKNOWLEDGMENTS

Support for PFH, DG, and XM was provided by an Alfred P. Sloan Research Fellowship, NASA ATP Grant NNX14AH35G, and NSF Collaborative Research Grant #1411920 and CAREER grant #1455342. Numerical calculations were run on the Caltech compute cluster “Zwicky” (NSF MRI award #PHY-0960291) and allocation TG-AST130039 granted by the Extreme Science and Engineering Discovery Environment (XSEDE) supported by the NSF.

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discrete steps. In the large GMCs where most stars form ($\sim 10^6 - 10^7 M_\odot$), this means that the first generation of stars formed can continue to alter the GMC properties while subsequent star formation occurs. However star formation in the smallest GMCs will be artificially “abrupt” (although GMCs with masses this low contribute negligibly to the variation in the IMF).

- Feedback processes from low-mass stars, e.g. protostellar outflows, are not explicitly included in the simulations. We only consider the effects of massive stars, which dominate on GMC scales provided there are sufficient stars to sample the IMF.
- The turbulent velocity dispersion in the code is calculated from using a kernel interpolation over the the relative velocities between the nearest ~ 32 resolution elements, after subtracting the coherent shear and contraction/expansion terms. This means that for very small GMCs with masses $\lesssim 10$ times the resolution, internal motions are not well-resolved. In this limit the general tendency is to underestimate the turbulent velocity dispersions (see e.g. the detailed turbulence studies in Hopkins 2015). But again, these do not contribute significantly in our predictions.
- The simulations do not explicitly follow non-equilibrium chemistry (e.g. molecular hydrogen formation/destruction), instead relying on pre-tabulated equilibrium cooling rates as a function of density, temperature, metallicity, and the strength of the local radiation field in several bands. It was shown by Hopkins et al. (2012) that these approximations have little to no effect on galactic star formation properties but they could conceivably alter the scatter in small-scale cloud properties.

ACKNOWLEDGMENTS

Support for PFH, DG, and XM was provided by an Alfred P. Sloan Research Fellowship, NASA ATP Grant NNX14AH35G, and NSF Collaborative Research Grant #1411920 and CAREER grant #1455342. Numerical calculations were run on the Caltech compute cluster “Zwicky” (NSF MRI award #PHY-0960291) and allocation TG-AST130039 granted by the Extreme Science and Engineering Discovery Environment (XSEDE) supported by the NSF.

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