Particle Simulation of the Generation of Plasmaspheric Hiss

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Abstract We have conducted a one-dimensional electromagnetic particle simulation with a parabolic magnetic field to reproduce whistler-mode hiss emissions in the plasmosphere. We assume a bi-Maxwellian distribution with temperature anisotropy for energetic electrons injected into the plasmosphere and find that hiss emissions are generated with spectrum characteristics typical of those observed by spacecraft near the magnetic equator. The hiss emissions contain fine structures involving rising tone and falling tone elements with variation in frequencies. The amplitude profile of the spectra agrees with the optimum wave amplitude derived from the nonlinear wave growth theory. The simulation demonstrates that hiss emissions are generated locally near the magnetic equator through linear and nonlinear interactions with energetic electrons with temperature anisotropy. The coherent hiss emissions efficiently scatter resonant electrons of 2.5–80 keV into the loss cone.

1. Introduction

Whistler-mode hiss is a commonly occurring electromagnetic emission in the Earth’s plasmasphere and plasmaspheric plumes. Dependent on local magnetic conditions, typical hiss frequencies range from ~100 Hz to several kHz, and amplitudes range from a few pT to hundreds of pT. There have been extensive observations of hiss dating from the earlier years of the satellite age to the present day (e.g., Hartley et al., 2018; He et al., 2019; Kim & Shprits, 2019; Li et al., 2013; Liu et al., 2020; Malaspina et al., 2017; Meredith et al., 2004, 2018; Nakamura et al., 2016, 2018; Ni et al., 2014; Smith et al., 1974; Su et al., 2018; Summers et al., 2008, 2014; Thorne et al., 1973, 1974, 1977; Tsurutani et al., 1975, 2015, 2018). Dependent on the location of the plasmapause and plasmaspheric plumes, hiss can efficiently pitch-angle scatter electrons in the energy range from ~10 keV to several MeV over all magnetic local time and the nominal L-shell range, 1.0 < L < 7. Thus, hiss is a primary agent for influencing the distribution and dynamics of electrons throughout the inner magnetosphere (e.g., Breneman et al., 2015; Li et al., 2014; Meredith et al., 2006; Ni et al., 2014; Summers et al., 2007a, 2007b; Thorne et al., 2013; Tsurutani et al., 1975, 2015, 2018). In fact, cyclotron resonant pitch-angle scattering by plasmaspheric hiss is considered responsible for the formation of the “slot region” (approximately 2.5 < L < 3) between the inner and outer electron radiation belts (Lyons & Thorne, 1973; Lyons et al., 1972).

The primary excitation mechanism of plasmaspheric hiss appears to be electron cyclotron resonance resulting from the primary injection of a distribution of anisotropic electrons into the magnetic equatorial plane. This generation mechanism for hiss was originally suggested in the early studies (e.g., Kennel & Petschek, 1966; Kennel & Thorne, 1967; Thorne et al., 1979); see also the more recent work by Cornilleau-Wehrlin et al. (1993), He et al. (2019), Kletzing et al. (2014), and Su et al. (2018). It is possible that lightning may also excite plasmaspheric hiss at frequencies of several kHz (e.g., Green et al., 2005). Bartnik et al. (2008) suggested a novel mechanism whereby distinct chorus waves originating outside the plasmasphere could propagate into the plasmasphere and evolve into hiss. However, Hartley et al. (2019), using observations from the Electric and Magnetic Field Instrument Suite and Integrated Science (EMFISIS) instrument on the Van Allen Probes, together with ray tracing simulations, find it unlikely that chorus could contribute significantly to plasmaspheric hiss wave power.

The study by Summers et al. (2014) was the first to identify and examine the fine structure of plasmaspheric hiss. Using waveform burst data from the EMFISIS instrument on eight 1 s samples, Summers et al. (2014)
demonstrated that plasmaspheric hiss is a coherent emission with complex fine structure. Moreover, hiss was seen to be characterized by short-time discrete, rising tone, and falling tone elements, similar to but different from whistler-mode chorus emissions. In a subsequent analysis, Omura et al. (2015) showed that previously developed nonlinear growth theory of chorus waves (Omura & Nunn, 2011; Omura et al., 2008, 2009) could be adapted to apply to hiss. It was found that instantaneous wave amplitudes constructed from the observed plasmaspheric hiss waveforms from Van Allen Probe A favorably matched the theoretically predicted optimum wave amplitudes and threshold values. Nakamura et al. (2016) further tested the nonlinear wave growth theory applied to hiss emissions and found good agreement between the observed frequency sweep rates for rising tone elements and the nonlinear theory. In a complementary study, Nakamura et al. (2018) surveyed 3 years (2013–2015) of Van Allen Probes data on plasmaspheric plume crossing events and found that 97% of the observed plumes were accompanied by hiss emissions. Detailed examination of the hiss spectra showed that whistler-mode hiss in plasmaspheric plumes universally possesses fine structure of the type found by Summers et al. (2014) in the plasmasphere itself.

In this paper, we carry out self-consistent particle simulations of plasmaspheric hiss. We modify the electromagnetic simulation used for chorus wave generation studies (Hikishima & Omura, 2012; Hikishima et al., 2009a, 2009b) to plasmaspheric conditions. As we shall show below, our simulation can reproduce very well the observed fine structure of plasmaspheric hiss reported above. In the following section, we describe the simulation method in detail. In section 3, we report the results, and in section 4, we provide discussion and state our conclusions.

2. Simulation Method

We perform a self-consistent electromagnetic full-particle simulation to study wave-particle interaction generating whistler-mode waves in the Earth’s inner magnetosphere using a code originally developed by (Hikishima et al., 2009a, 2009b). The simulation system is a one-dimensional model taken along the ambient magnetic field near the equator of the Earth’s dipole magnetic field. The ambient magnetic field line takes a nonuniform dipole field near the equatorial region, which is represented by a parabolic function $B = B_0(1 + ah^2)$, where $h$ is the distance along the field line and $B_0$ is the magnitude of the ambient magnetic field.
3. Results

3.1. Generation of Hiss Emissions

In Figure 1a, we plot frequency spectrograms of the transverse magnetic wave field $B_w$ at different locations $h = -100, -50, 0, 50, 100 \text{ cm}^{-1}$ along the field line. The overall time interval of the power spectrograms corresponds to $10 \text{ s}$ at $L = 4$. The field data are stored over a time interval $\Delta t = 2.05 \text{ s}$ in the simulation. We apply the fast Fourier transform (FFT) with a Hann window using 2,048 data points corresponding to a time duration $4.194 \text{ s}$ (51.3 ms) in an FFT frame shifted by $65.5 \text{ cm}^{-1}$ (0.8 ms) at each time interval $\Delta t$.

A long-time simulation run was performed, starting from the initial velocity distribution function of anisotropic energetic electrons. Short electromagnetic emissions are steadily generated. Since the wave frequency is below the electron cyclotron frequency $\Omega_{eo}$, with an electron plasma frequency $15 \Omega_{eo}$, the electromagnetic fields comprise whistler-mode waves that can interact with energetic electrons.

Using the spatial helicity of whistler-mode waves, we can separate the waves into two groups propagating forward and backward along the ambient magnetic field, as plotted in Figures 1b and 1c. The banded waves are generated at the equatorial region through local cyclotron resonance with anisotropic energetic electrons. The growing wave spectrograms over the long time scale $8 \times 10^3 \text{ s}$ show unstructured broadband emissions which are characterized as whistler-mode hiss emissions. The emissions exhibit a common feature of plasmaspheric hiss, that is, broadband waves at frequencies $\omega < 0.1 \Omega_{eo}$ and with a sudden decrease of the wave power in the lower frequency part ($\omega < 0.02 \Omega_{eo}$) (Bortnik et al., 2008; Nakamura et al., 2018; Summers et al., 2010).
et al., 2014). The banded emissions have a peak intensity around $\omega = 0.03 \Omega_{eo}$ corresponding to several tens of pT at $L = 4$ (Meredith et al., 2004; Thorne et al., 1973).

Over the whole region ($h = -100$ to $100$ cm$^{-1}$) around the equator, the banded structure of the waves is formed in the frequency range of $\omega < 0.1 \Omega_{eo}$. Both forward and backward waves, after the separation of propagation direction, show that short narrow-band wave packets with rising and falling tone frequencies are generated around the equator. These wave packets are amplified through propagation from the equator to higher latitude by interacting with counterstreaming energetic electrons. This result indicates importantly that the source region of the plasmaspheric hiss emissions is the equatorial region.

Figure 2 shows that the initial wave growth stage ($t = 0$ to $8 \times 10^4 \Omega_{eo}^{-1}$) of waves propagating forward in Figure 1 corresponds to time duration of 1 s. By comparing the spectrograms monitored at different locations $h = -100, -50, 0, 50, 100$ cm$^{-1}$ along the magnetic field line, we find that the waves grow near the magnetic equator within a short distance. The substantial difference in wave amplitudes at locations $h = 0$ and $h = 50$ in Figure 2 is due to a large convective wave growth rate. The same wave growth process is found in the backward waves, as we see in Figure 1.

Further, we find enhanced wave amplitudes around $\omega = 0.05 \Omega_{eo}$. These waves undergo convective wave growth during propagation toward higher latitude, and the frequency band becomes wider. Each of the wave packets is due to a nonlinear process under a coherent wave packet with a frequency variation. These wave packets with rising and falling tones form fine structures growing in space as shown in Figure 2.

### 3.2. Fine Structure of Hiss Emissions

In Figure 3, we have enlarged the dynamic wave spectrogram, modifying the resolution of the spectrogram (see the dotted box in Figure 2e). The sampling time of the field data is $\Delta t = 4.10 \Omega_{eo}^{-1}$. We apply an FFT with the Hann window using 1,024 data points corresponding to a time duration $4.194 \Omega_{eo}^{-1}$ (51.3 ms) in an FFT frame, and the frame is shifted by $131 \Omega_{eo}^{-1}$ (1.6 ms). The simulation is started from the initial thermal noise determined by the initial distribution of energetic and cold electrons. The wave packets grow in a short time scale of $t = 1 \times 10^4 \Omega_{eo}^{-1}$ corresponding to 0.12 s. We find elements of the waves grow with frequency variations resulting in fine structures in the dynamic spectrogram representative of the nonlinear wave growth process. This is essentially the same as the generation process of chorus wave emissions.

Figure 4 shows the space and time evolution of the wave amplitudes and frequencies of the transverse magnetic fields of the forward- and backward-traveling waves. Many wave packets forming lines with red colors in Figure 4a are formed, and they travel along the magnetic field with different group velocities, indicating wave packets are generated at many different frequencies of the broadband waves. Figure 4b shows the space-time evolution of the wave frequency determined from the phase variation of the transverse wave magnetic field with time step $4.10 \Omega_{eo}^{-1}$. The different fine colors indicate the wave generation processes take place at different frequencies. Frequencies of the wave packets are constant during their propagation, as indicated by the same colors in Figure 4b. The wave packets also undergo substantial convective growth as a result of propagation away from the magnetic equator. The lines with dark blue color in Figure 4b correspond to wave packets with frequencies $\omega \leq 0.1 \Omega_{eo}$ and their wave amplitudes become larger in space and time through propagation as shown in Figure 4a.

Figure 5a presents an averaged amplitude of the transverse magnetic wave field $B_{te}$ in the equatorial region $-20 < h < 20$ cm$^{-1}$. Wave packets are excited near the equator through cyclotron resonance. Figure 5b is the initial stage ($t = 0$ to $1 \times 10^4 \Omega_{eo}^{-1}$) of the simulation. The blue and red lines represent temporal evolution of theoretical wave amplitudes calculated from linear wave growth rates (plotted in Figure 6) at $\omega = 0.03 \Omega_{eo}$ and $0.06 \Omega_{eo}$. These frequencies are chosen with reference to the maximum linear growth rate which occurs at $\omega = 0.06 \Omega_{eo}$. After initiation of the simulation run,
whistler-mode waves around the equator grow from a thermal fluctuation of the anisotropic energetic electrons following an amplification consistent with the linear wave growth rate up to $t = 0.2 \times 10^4 \Omega_e^{-1}$. The wave growth after $t = 0.2 \times 10^4 \Omega_e^{-1}$ is nonlinear because the wave spectra develop fine structures with large amplitudes, as shown in Figure 2. Each of the fine structures grows at the nonlinear growth rate which is greater than the linear growth rate, as shown in Figure 6. The wave amplitude in Figure 5 shows much smaller growth, because it is calculated by averaging the wave amplitudes in the equatorial region $(-20 < h < 20 \ c\Omega_e^{-1})$, while the fast growing wave packets are much localized in space and their contribution to the averaged value is limited.

We plot the linear wave growth rate and the nonlinear wave growth rates at the threshold and optimum wave amplitudes as function of wave frequency. Above the threshold wave amplitude, waves can grow at
a fixed position near the equator as an absolute instability (Omura et al., 2009). While a wave above the threshold amplitude grows with a varying frequency, the wave amplitude cannot exceed much above the optimum amplitude, which satisfies the condition for the most efficient energy transfer from resonant electrons moving around the nonlinear trapping wave potential (Omura & Nunn, 2011). The linear wave growth rate is computed by Kyoto University Plasma Dispersion Analysis Package (KUPDAP) (Sugiyama et al., 2015) based on the plasma parameters of the simulation run listed in Table 1. Interestingly, the linear growth rate has a peak in the frequency at $\omega \sim 0.05 \Omega_{e0}$ which depends on plasma parameters, while the nonlinear wave growth is larger than the linear wave growth in the higher frequency range.

We have extracted one of the hiss elements undergoing convective growth by choosing a frame of reference moving with the group velocity of the hiss element, as shown in Figure 7a. We calculated average values of the wave amplitude and instantaneous frequency of the wave packet by taking a short time window $\Delta t = 100 \Omega_{e0}^{-1}$. The instantaneous frequency is the averaged value of frequencies calculated from a phase variation of dominant wave amplitudes within the time window $\Delta t$. As shown in Figures 7b and 7c, the frequency of the wave packet is nearly constant, while the amplitude increases gradually as the wave packet moves away from the equator. While the wave amplitude increases linearly as a function of distance from the equator, the gradient of the parabolic magnetic field also increases linearly. The inhomogeneity factor $S$ (Equation 10 in Omura et al., 2009), comprising the major term containing the gradient of the magnetic field divided by the wave amplitude, can maintain the optimum value $-0.4$ for wave growth. As we find in Figure 7b, the convective wave growth subsides when the flux of the resonant electrons decreases. This is due to the adiabatic variation of the electron flux to smaller values of the parallel velocities as well as the shift of the resonance velocity to a larger value at a larger distance from the equator. From the spatial variation of $B_{W0}$, the growing wave packet over $h = 50 \sim 100 c \Omega_{e0}^{-1}$ shown in Figure 7b and from the group velocity $V_{g} = 0.05 c$ evaluated from Figure 7a, we can calculate the temporal growth rate as $\Gamma_{g} = 0.7 \times 10^{-3}$, which is in good agreement with the nonlinear growth rate plotted in Figure 6. The maximum amplitude of the wave packets varies in a range of $80 \sim 200$ pT depending on a distance from the equator as shown in Figure 7b.

To study the dependency of the wave packet amplitude on the wave frequency, we apply a band-pass filter with a frequency width of $0.01 \Omega_{e0}$ to a time sequence ($t = 0 \sim 8 \times 10^{-4} \Omega_{e0}^{-1}$) of the wave field values observed at the equator. After applying the band-pass filter, we produce a waveform at each bin of the frequency band by taking an inverse FFT. We plot the instantaneous frequency calculated from a time variation of the transverse wave magnetic fields $B_{W0}$ and the instantaneous wave amplitude by each dot in Figure 8a. We plot the theoretical optimum and threshold amplitudes in Figure 8b. By changing the parameter $Q$, which is the depth of the electron hole formed by the coherent potentials of the hiss emissions (Omura et al., 2008), we found that the profile of the optimum and threshold wave amplitudes shows reasonable agreement with $Q = 0.05$. As shown in Figures 1 and 2, the wave in a range of $\omega \geq 0.1 \Omega_{e0}$ contains thermal fluctuations. Because of the limited number of super particles in the simulation, the wave amplitude does not agree with the optimum amplitude in the higher frequency range $\omega \geq 0.1 \Omega_{e0}$.

Figure 5. (a) Temporal evolution of the averaged transverse magnetic wave amplitude (natural logarithm scale) around the equator ($-20 < h < 20 \times \Omega_{e0}^{-1}$). The shaded area is shown in panel (b). (b) The initial stage ($t = 0 \sim 10 \times \Omega_{e0}^{-1}$) of wave growth from thermal fluctuations. The blue and red lines show the wave amplitude calculated from theoretical linear wave growth rates at $\omega = 0.03 \Omega_{e0}$ and $0.06 \Omega_{e0}$, respectively.

Figure 6. (Red) linear wave growth rate $\gamma/\Omega_{e0}$, (black) nonlinear wave growth rate $\Gamma_{N}/\Omega_{e0}$ evaluated from the threshold amplitude, and (blue) nonlinear wave growth rate evaluated from the optimum amplitude as functions of wave frequency.
3.3. Precipitation of Resonant Electrons

Figure 9 shows the velocity distribution function $f(v_{\parallel}, v_{\perp})$ of the energetic electrons near the magnetic equator ($h \sim 0.1 c\Omega_{e0}^{-1}$) plotted at different times ($t = 0.5 \times 10^5, 1.0 \times 10^5,$ and $5.9 \times 10^5 \Omega_{e0}^{-1}$). The initial velocity distribution ($t = 0 \Omega_{e0}^{-1}$) is a subtracted bi-Maxwellian forming the loss cone with the typical size of $L = 4$. Energetic particles are in resonance with hiss elements at a wide range of resonance velocities of both forward- and backward-propagating waves. In Figure 9, energetic electrons with a positive parallel velocity ($v_{\parallel}$) are shown, which are caused by backward-propagating hiss waves. The hiss waves transport energetic electrons over the range $v_{\parallel} = 0.1 - 0.5 c$ into the loss cone indicated by the white dashed line. The corresponding energy of the electrons is 2.5–80 keV. The present simulation result demonstrates that hiss waves with wave frequency $\omega < 0.1 \Omega_{e0}$ can scatter electrons of tens of keV energy into the loss cone in a plasma environment with the cold plasma frequency $\omega_{pe} = 15 \Omega_{e0}$.

4. Summary and Discussion

We have performed a self-consistent electromagnetic full particle simulation around the magnetic equator with a dipole field which is approximated by a parabolic function. In order to reproduce plasmaspheric hiss emissions, we set up anisotropic energetic electrons that resonate with whistler-mode waves assuming plasmaspheric parameters. The simulation shows that wave packets are generated through linear and nonlinear interactions with anisotropic energetic electrons that then propagate away from the equator by means of convective growth. The fine structures span a broadband within $\omega < 0.1 \Omega_{e0}$, which is typical of hiss emissions observed by many satellites. The spectra of the hiss emissions show a frequency variation containing rising and falling tones, characteristic of nonlinear wave growth. The coherent hiss emissions resonate with energetic electrons and scatter them into the loss cone.

Table 1

| Parameter                              | Value          |
|----------------------------------------|----------------|
| Time step:                             | $0.004 \Omega_{e0}^{-1}$ |
| Grid spacing:                          | $0.01 c\Omega_{e0}^{-1}$ |
| Plasma frequency of cold electrons: $\omega_{pe}$ | $15 \Omega_{e0}$ |
| Density ratio of hot electrons to cold electrons: | $4 \times 10^{-4}$ |
| $N_h/N_c$                              |                |
| Total number of cold electrons         | 33,554,432     |
| Total number of energetic electrons    | 67,108,864     |
| Coefficient of parabolic magnetic field: $\alpha$ | $1.86 \times 10^{-7} \left(1 - \Omega_{e0}^{-1}\right)^2$ |
| Thermal velocity of hot electrons at the equator: | $0.23 c, 0.36 c$ |
| $v_{h,L} - v_{h,L}$                    |                |

Figure 7. (a) Enlarged view of time-space evolution of transverse wave magnetic field $B_w$ indicated by the dotted box in Figure 4a. Spatial profiles of (b) wave amplitude (c) averaged frequency of the wave packet indicated by the arrow.
Figure 8. (a) Amplitudes and instantaneous frequencies of forward-traveling hiss waves at the equator. These are calculated from waveforms obtained by IFFT after applying a band-pass filter with width $\Delta \omega = 0.01 \Omega_{eo}$ in the wave frequency spectrum at the equator over the interval $t = 0-8 \times 10^4 \Omega_{eo}^{-1}$. (b) The threshold wave amplitude and optimum amplitude with parameters $\tau = 0.5$ and $Q = 0.05$ plotted in red and blue, respectively.

Figure 9. Velocity distribution function $f(V_{\parallel}, V_{\perp})$ of energetic electrons near the equator at the times $t = 0$, $0.5 \times 10^5$, $1.0 \times 10^5$, and $5.9 \times 10^5 \Omega_{eo}^{-1}$. The white dashed lines indicate the loss cone angle.
Even with modest temperature anisotropy (A ~ 1.4), which gives relatively small linear growth rates, efficient scattering of energetic electrons to lower pitch angles takes place near the equator, transferring kinetic energy to electromagnetic wave energy. This typifies nonlinear coherent wave-particle interaction. Because of the wide band spectra, the resonance velocity varies over a wide range, and electrons at many different pitch angles can be in resonance with the hiss waves. Multiple coherent interactions can take place at different pitch angles, effectively transferring the energetic electrons to lower pitch angles and precipitating the energetic electrons into the loss cone.

In the present simulation, we assume energetic electrons with a given temperature anisotropy as an initial condition, and an additional fresh energy source is not provided. However, in practice, energetic electrons are continuously transported into the plasmapause owing to the dawn-to-dusk electric field. The injected electrons into the equatorial region contribute to continuous generation of hiss emissions. A more realistic simulation model with continuous injection of energetic electrons would further improve our understanding of the characteristics of hiss emissions.

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