Learning to Manipulate Amorphous Materials

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We present a method of training character manipulation of amorphous materials such as those often used in cooking. Common examples of amorphous materials include granular materials (salt, uncooked rice), fluids (honey), and visco-plastic materials (sticky rice, softened butter). A typical task is to spread a given material out across a flat surface using a tool such as a scraper or knife. We use reinforcement learning to train our controllers to manipulate materials in various ways. The training is performed in a physics simulator that uses position-based dynamics of particles to simulate the materials to be manipulated. The neural network control policy is given observations of the material (e.g. a low-resolution density map), and the policy outputs actions such as rotating and translating the knife. We demonstrate policies that have been successfully trained to carry out the following tasks: spreading, gathering, and flipping. We produce a final animation by using inverse kinematics to guide a character’s arm and hand to match the motion of the manipulation tool such as a knife or a frying pan.

CCS Concepts: • Computing methodologies → Animation; Reinforcement learning; Control methods.

Additional Key Words and Phrases: Character control, reinforcement learning, physics simulation, deformable materials.

ACM Reference Format:
Yunbo Zhang, Wenhao Yu, C. Karen Liu, Charles C. Kemp, and Greg Turk. 2020. Learning to Manipulate Amorphous Materials. ACM Trans. Graph. 39, 6, Article 189 (December 2020), 11 pages. https://doi.org/10.1145/3414685.3417686

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1 INTRODUCTION

People can manipulate materials that have a wide variety of physical properties, and we would like our virtual characters to be similarly skilled at manipulation. One broad class of materials that has received little attention for character animation are materials that have no fixed shape, so-called amorphous materials. Amorphous materials include granular materials, fluids, and visco-plastics. Our goal is to develop character control policies for manipulating such amorphous materials. In day-to-day living, the foods that we cook in our kitchen provide numerous examples of such materials. Examples of manipulating amorphous materials in the kitchen include spreading butter on toast, gathering fried rice into a pile to be served, and flipping pancakes or burgers on a skillet.

Rather than creating hand-written controllers for our characters, we draw upon the strengths of reinforcement learning algorithms to develop robust character control policies. Researchers have successfully applied reinforcement learning to create policies that control characters to perform a variety of motor skills such as parkour [Peng et al. 2018], basketball dribbling [Liu and Hodgins 2018], ice skating [Yu et al. 2019] and dressing [Clegg et al. 2018].

We separate the character control task into two parts. First, we use reinforcement learning to train a material manipulation policy (e.g. spreading rice) that describes the motion of a tool such as a knife or a frying pan. The character’s body is not considered during the training of the tool motion. Second, when producing a final animation, we use inverse kinematics to guide the arm and hand of a character so that it matches the motion of the tool as the material is being manipulated.

Numerous character animation controllers have been created for picking up, moving and placing rigid objects. When interacting with such a discrete rigid object, the object’s position and orientation require just six numbers. In contrast, creating observations of amorphous materials for a character requires a more verbose object description. Consider, for example, rice that is on the heated surface that is being cooked by a hibachi chef. The rice might be scattered across the heat surface or may be heaped in one or more
piles. When manipulating such materials, our animated characters need to be able to recognize and act in different ways based on the rice’s configuration. We have chosen to describe a given material using either a material density map or a depth image, which gives the character policy a rich description of the configuration of the material. Furthermore, we find that the coordinate frame of these image maps has a large effect on the speed at which a controller will learn a task. In particular, we find that for the tasks we investigated, tool-centric observations are superior to observations in world-space.

Another way in which characters acting upon amorphous materials differs from other animation tasks is the quantitative evaluation of a given action. When using reinforcement learning for common tasks such as locomotion, the general nature of a reward function is well known. A typical reward function might be a term for distance travelled, a balance term, and an energy term. Similarly, reward terms for reaching out a robotic arm to a given object are commonplace. However, we have found no such ready-made rewards in the research literature for tasks such as scattering or gathering granular materials. Much of our effort has been devoted to discovering effective ways in which to reward a given character policy for such tasks.

A challenge to using reinforcement learning for amorphous material manipulation is that simulating amorphous materials comes at a high computational cost. We address this problem by using the FleX simulator, which is capable of simulating a wide range of materials using a position-based particle model [Macklin et al. 2014]. When simulating the manipulation of materials, we use FleX to perform several rollouts simultaneously in a single simulation environment on the GPU, similar to the work of Chebotar et al. on robot training in simulation [2019].

2 RELATED WORK
Controlling simulated characters and robots to exhibit complex and versatile manipulation skills is a long-standing challenge in computer animation, robotics, and machine learning. Researchers have investigated a large variety of manipulation problems that span different types of objects and end effectors such as object grasping [Andrews and Kry 2012; Kalashnikov et al. 2018; Liu 2009; Zhao et al. 2013], in-hand manipulation [Akayka et al. 2019; Bai and Liu 2014; Mordatch et al. 2012; Ye and Liu 2012], cloth folding and manipulation [Bai et al. 2016; Miller et al. 2012; Wu et al. 2019], and scooping [Park et al. 2019; Schenck et al. 2017]. Many of these works leverage trajectory optimization algorithms to synthesize the manipulation motion. For example, Bai et al. developed an algorithm to find a trajectory where a piece of cloth or garment was manipulated into desired states through contact forces [2016]. However, these methods are usually specific to a particular motion and require frequent re-planning of the motion in order to combat uncertainties and perturbations in the environment.

Deep reinforcement learning (DRL) provides a general framework for characters to automatically find a control policy from rewards that can effectively handle uncertainties and perturbations in the system. Recent advancements in DRL algorithms have enabled researchers to create control policies for a variety of character motor skills [Lee et al. 2019; Liu and Hodgins 2018; Peng et al. 2018; Yu et al. 2019], including ones for manipulation problems such as solving rubik’s cube [Akayka et al. 2019] and opening doors [Rajeswaran et al. 2017]. However, due to the high sample complexity of DRL algorithms and the high computation time for non-rigid objects like fluids and cloths, it is most common to apply DRL algorithms to manipulation problems with rigid objects, for which stable and efficient simulation tools are available [Coumans and Bai 2016; Lee et al. 2018; Todorov et al. 2012]. For the work that do apply DRL algorithms to manipulating non-rigid objects, some form of prior knowledge about the task or the object is usually utilized to make the problem more tractable [Clegg et al. 2018; Elliott and Cakmak 2018; Ma et al. 2018; Wilson and Hermans 2019; Wu et al. 2019]. For example, Clegg et al. applied DRL to teach a simulated humanoid character to dress different garments [2018]. To make the dressing problem manageable, they decomposed the dressing motion into a set of more manageable sub-tasks, which requires manual effort for new dressing problems. More recently, Wu et al. proposed a DRL-based approach for manipulating cloth and ropes from visual input [2019]. They assumed the robot to alternate between picking and placing the object during the manipulation and developed a learning algorithm that is suitable for this action space.

Ma et al. proposed a learning system for using fluid to control rigid objects [2018]. They learned an auto-encoder for extracting compact features from the input image, which is used as the observation space in training the control policy. Our work can be viewed as solving an opposite problem: we actuate a rigid object such as a pan or a spatula to manipulate the state of amorphous materials. We do not use an auto-encoder stage in our network architecture, but instead use a two-stage convolutional neural network to process the images that represent the state of the materials.

Another way to deal with the high computation complexity of non-rigid objects for efficient learning is to use a differentiable representation of the objects’ dynamics. Researchers have proposed to represent the dynamics model using deep neural networks [Li et al. 2019; Schenck and Fox 2018; Schenck et al. 2017]. For instance, Schenck et al. formulated the position-based dynamics algorithm as neural network operations that can be embedded inside a bigger neural network [2018]. Li et al. developed a graph network-based approach for representing the dynamics of particle-based objects [2019]. They show their method on manipulating fluid and deformable objects such as making a rice ball. The success of these methods usually relies on being able to collect training data that are relevant to the task of interest, limiting them to relatively simple forms of tool-object interactions. Alternatively, researchers have also investigated formulating and implementing physics of these objects in a differentiable way [Hu et al. 2019a,b]. These methods have great potential in achieving effective learning for complex materials. However, it can be non-trivial and requires human expertise to create such a model for new problems that involve novel materials and interactions.

3 METHODS
In this section, we present our pipeline for training policies that control tools to manipulate amorphous materials. We will first give
an overview of the reinforcement learning control problem formulation. We will then introduce our representation for the material states and discuss our controller design. We next discuss policy training details and our simulation environment. Lastly, we describe how we generate a character animation from a trained policy.

3.1 Policy Training Formulation
We use reinforcement learning to train our control policies for manipulation. We use a neural network to represent the policy, and this network’s input is the observed state of the material and the manipulation tool, and the output is the tool motion (the action). To train the policy, we run many different trajectories, and after each action a reward is given that is used to tune the weights of the neural network.

More formally, we formulate our control problem as a Markov Decision Process (MDP) defined by the tuple \((S, \mathcal{A}, T, r, \rho_0, \gamma)\). \(S\) is the state space of the environment, \(\mathcal{A}\) is the action space, \(T(s_t, a_t) = s_{t+1}\) is the transition function (the simulation of the environment) that generates a new state \(s_{t+1}\) given a state action pair \((s_t, a_t)\), \(r(s_t, a_t)\) is the reward function evaluating the quality of a state action pair, \(\rho_0\) is the initial state distribution, and \(\gamma \in [0, 1]\) is the discount factor. The goal is to find an optimal control policy \(\pi_0\), that by solving for \(\theta\), maximizing the following sum of expected rewards over a distribution of all trajectories \(\tau = (s_0, \pi(s_0), \ldots, \pi(s_T), s_T)\).

\[
R(\theta) = \mathbb{E}_\tau \left[ \sum_{t=0}^{T} \gamma^t r(s_t, a_t) \right]
\]

(1)

3.2 Material State Representation
The state space \(S\) of our problem contains information of the controlled tool as well as the state of the amorphous material. Training the control policy with full state information of the material as input, e.g. positions and velocities of all the particles in a granular material, is not practical due to the high dimensionality of the material state. It also limits the policy to a fixed material setting, e.g. the same number of particles. Using the image of the scene as input can allow the policy to generalize to different materials, yet it does not generalize to similar materials but with different appearances. In this work, we represent the material state for input to the policy using a 2D grid of values that summarize the density and/or height of the simulated materials at each grid point. This allows the policy to quickly adapt to novel materials with minimal change.

3.2.1 Density Map. In our work, we represent the simulated material as particles. We denote the position of each particle as \(x_{\text{mat}}^p\), where \(p \in \{0, 1, \ldots, P\}\) is the index of the particle among the total \(P\) particles. To estimate the density of the material, we take an Eulerian view by discretizing the 2D ground plane into an \(N \times N\) grid with cell width \(h\) and store density information on the grid as \(D \in \mathbb{R}^{N \times N}\), where each value \(D(i, j)\) on the grid measures the density of material at the position of grid cell \((i, j)\). We denote the position of grid cell \((i, j)\) as \(x_{\text{grid}}^{i,j}\). We further write the vector from a grid cell center \((i, j)\) to a particle \(p\) as \(v^{p,i,j} = x_{\text{mat}}^p - x_{\text{grid}}^{i,j}\). We compute the density at a certain point \(D(i, j)\) as:

\[
D(i, j) = \sum_{k \in K(i,j)} w(k, i, j),
\]

(2)

\[
w(k, i, j) = \sqrt{(2.5h - |v^{k,i,j}[0]|)^2 + (2.5h - |v^{k,i,j}[1]|)^2},
\]

(3)

where \(K(i,j)\) is the set of indices for the particles that lie within the grid cell \((i, j)\) and its two-ring neighbors, i.e. \(|v^{k,i,j}[d]| < 2.5h\) for \(d \in \{0, 1\}\).

3.2.2 Height Map. Similar to the density map, we approximate the average height of the material using a 2D height map \(H \in \mathbb{R}^{N \times N}\). Using the same weight function \(w\) defined above, the height value at each grid cell \((i, j)\) is computed as \(H(i, j) = \frac{\sum_{p \in K(i,j)} y^p w(p,i,j)}{D(i,j)}\), where \(y^p\) is the height of the \(p\)th particle.

3.2.3 Relative State Representation. In many manipulation tasks it is more important to reason about the relative pose between objects of interest rather than their absolute locations in the global coordinate. For example, when assembling two lego pieces, it is crucial that they are aligned relative to each other, and it is less important what orientation or position they are in. Following this intuition, we propose to represent the state of the material in the local coordinate frame of the tool. We first extract the pose of the tool as a homogeneous transformation matrix \(A\) from the global coordinate frame. We then transform the positions of all the particles in the material into the local space of the tool: \(\hat{x}_{\text{mat}}^p = A^{-1}x_{\text{mat}}^p\). Then we use the local particle positions to compute the density map \(D\) and height map \(H\) as shown in Figure 2.

3.3 Controller Design

3.3.1 Observation Space. We construct our observation as \(O = [O_{\text{mat}}, O_{\text{tool}}]\), where \(O_{\text{mat}} \in \mathbb{R}^{N \times N \times M}\) includes the material information as well as certain task-related information such as goal location. The number of input channels \(M\) depends on the task and is discussed in more detail in Section 4. \(O_{\text{tool}}\) contains the position and orientation information of the tool defined as \(O_{\text{tool}} = [x_{\text{tool}}, \cos(t_{\text{tool}}), \sin(t_{\text{tool}}), x_{\text{tool}}, \cos(t_{\text{tool}}), \sin(t_{\text{tool}})]\), where \(x_{\text{tool}}\) is the position of the tool and \(t_{\text{tool}}\) is the Euler angles representing the orientation of the tool. The dimensions of \(x_{\text{tool}}\) and \(t_{\text{tool}}\) depends on the tool and action space used for the task. For the angular velocity information, we use its sine and cosine value. There is a unique pair of values for the sine and cosine of the angular velocity because the angular velocity of the tool always stays in the range of \([-\pi, \pi]\) in the simulations.
optimization loss is defined in the following form:
and the previous policies within the trust region. The combined
man et al. 2017] to optimize our control policy. As an on-policy
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3.4 Policy Training
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3.3.3 Controller Structure. Our observation space is a combination of
2D images and accurate tool state, thus it is natural in the design of
the policy architecture to extract features of the two parts separa-
ately using different neural network blocks. For the image-based
observation part, convolution layers are well suited to extract lower
dimensional features. For the tool observation part, fully connected
layers are used to extract the information. Hence, our neural net-
work controller is designed as shown in Figure 3. To extract the
low dimensional feature from the images, we pass several 32 × 32
images through two convolutions layers with max pooling followed
by a single fully connected layer with 32 hidden units. The resulting
feature vector is then concatenated with \( O_{\text{tool}} \) and passed into two
fully connected layers each with 64 hidden units. To encourage
identification of positional information in the input images, our first
convolution layer \( \text{conv}0 \) uses the CoordConv layer design proposed in [Liu et al. 2018]. We used the ReLU functions as our activation
function for all output of convolution layers and fully connected
layers.

3.4 Policy Training
In this work, we use the proximal policy optimization (PPO) [Schul-
mus et al. 2017] to optimize our control policy. As an on-policy
algorithm, by sampling trajectories using the current policy, PPO
aims to find an improved policy by optimizing a surrogate loss func-
tion as well as trying to keep the KL-divergence between the current
and the previous policies within the trust region. The combined
optimization loss is defined in the following form:

\[
L_{\text{PPO}}(\theta) = L_{\text{Starr}} + L_{KL}
\]

\[
= -E_{\mathcal{D}} \left[ \min(r(\theta)A_t, \text{clip}(r(\theta), 1 - \epsilon, 1 + \epsilon)) \right] 
- \beta E_{\mathcal{D}} \left[ KL \left[ \pi_\theta(\cdot|s_t) \| \pi_{\theta_{old}}(\cdot|s_t) \right] \right],
\]

where \( r_\theta = \frac{\pi_\theta(a|s)}{\pi_{\theta_{old}}(a|s)} \) is the ratio of likelihood between the two
policies, \( A_t \) is the generalized advantage estimation (GAE) proposed in [Schulman et al. 2015], and \( \beta \) is a dynamically adjusted coefficient
to constrain the KL-divergence. We use a discount factor \( \gamma = 0.99 \)
across all of our training runs.

The FleX physics simulator that we use can simulate a large collect-
on of particles while running on a single GPU. To take advantage
of this compute power we run many rollouts at once on the GPU.
Specifically, we simulate a 7 × 7 grid of individual rollouts in FleX,
all of which are controlled by the actions generated from the policy
at the current iteration. In total, we sample 49,000 simulation steps
and use 64 samples per batch and use 10 epochs in every training
iteration.

3.5 Simulation
We simulate a one-way coupling system where a kinematic tool is
controlled to interact with amorphous material and the material
does not affect the motion of the tool. With FleX, we use position-
based dynamics (PBD) [Macklin et al. 2014] to simulate the material
as a collection of \( P \) particles with positions \( x^p_{\text{mat}} \). FleX provides
a rich set of materials and is highly efficient, making it well suited for
our task.

The manipulation tool is simulated as a kinematic object with a
state vector \( s = [q, \dot{q}] \) where \( q = [x, y, z, \phi, \psi, \theta]^T \) are the position
and orientation in Euler angles of the tool and \( q \) are the corre-
sponding time derivatives. To control the tool, a target position and
orientation vector \( \hat{q} \) is provided by the policy at each time step,
and an acceleration vector \( \ddot{q} \) is computed using a PD-controller as

\[
\ddot{q} = k_p (q - \hat{q}) - k_d \dot{q},
\]

where \( k_p \) and \( k_d \) are the gain and damping terms. Using the acceleration vector, the state of the tool is explicitly integrated as

\[
\begin{pmatrix}
q_{t+1} \\
\dot{q}_{t+1}
\end{pmatrix} =
\begin{pmatrix}
q_t \\
\dot{q}_t
\end{pmatrix} + \Delta t \begin{pmatrix}
\ddot{q}_t \\
\dot{q}_t
\end{pmatrix},
\]

where \( \Delta t \) is the simulation time step. By controlling the tool through
this higher-order integration process instead of directly modifying
its state, we obtain smoother motion of the tool.

In our experiments, we use three types of materials for demon-
strating our learning algorithm: granular material, visco-plastic
material, and viscous fluid material. Simulating granular and vis-
cous fluid materials can be done directly in FleX using existing
simulation models [Macklin et al. 2014]. However, the existing ma-
terials in FleX does not support effective simulation of visco-elastic
materials, thus we created our own visco-plastic model in FleX.

3.5.1 Visco-plastic Material Modeling. We want the visco-plastic
material to be able to recover from small deformations, not returning
to its former shape if it undergoes a large deformation. Also, when
experiencing extreme stretching, we expect the material to split, and
when compressed, separate pieces of material should merge. We
simulate these behaviours by dynamically creating, adjusting, and
removing a list of virtual springs \( s_{i,j} \) with rest lengths \( L_{i,j} \) among
the particles, where \( i \) and \( j \) denote the indices of the particles that
the spring connects. We define the following values \( d_m, d_p, r_c, r_s \),
where \( d_m \) and \( d_p \) are distance thresholds that determine merging
or breaking materials, \( r_c \) and \( r_s \) are ratio thresholds that determine

Algorithm 1: Visco-plastic Material Modeling

1: for Each spring $s_{i,j}$ do
2: \[ d = ||x^i_{mat} - x^j_{mat}|| \]
3: if $d < d_b$ and not cut by tool then
4: \[ L_{i,j} = \text{RestLengthUpdate}(d, L_{i,j}) \]
5: else
6: Delete $s_{i,j}$
7: end if
8: end for
9: for Every pair of particles with position $x^i_{mat}$ and $x^j_{mat}$ do
10: \[ d = ||x^i_{mat} - x^j_{mat}|| \]
11: if $d < d_m$ and not cut by tool then
12: if $s_{i,j}$ does not exist then
13: Create $s_{i,j}$ with $L_{i,j} = d$
14: end if
15: end if
16: end for

Algorithm 2: RestLengthUpdate

1: Input: Current particle distance $d$, Current spring rest length $d_{rest}$
2: \[ r_t = \frac{d}{d_{rest}} \]
3: if $r_t \leq r_c$ or $r_t \geq r_s$ then
4: return: $d$
5: else
6: return: $d_{rest}$
7: end if

when to plastically deform. Algorithm 1 describes how the rest lengths of the springs are updated and how the springs are created or removed. After determining the states of the springs, we simulate them in FleX as distance constraints.

4 RESULTS

We demonstrate three different material manipulation tasks: gathering, spreading, and flipping. Table 1 lists the different tasks and their training time. Note that even with GPU acceleration, training usually requires a full day or more. We discuss each of these tasks below, and animations are included in the accompanying video.

4.1 Gathering

In this task, various clusters of material are placed across the surface of a flat table. The task is to slide a hibachi scraper across the table in order to gather the material at a specified goal position. Figures 4, 5, and 6 show sequences of applying a policy to gather visco-plastic, granular, and viscous fluid materials.

The material observation space $O_{mat}$ consists of two images: a density map of the material, and a goal location map showing the location of the goal. For the motion of the scraper, we constrain its pose so that it can only slide on the table surface and rotate around the vertical axis. The translational states $x_{\text{tool}}$ and $\dot{x}_{\text{tool}}$ are $2D$ vectors storing the tool position and velocity on the plane.
We compute $r_t$ with granular material was unable to learn to gather more than a threshold, we advance the training to a new curriculum by keeping adding clusters until the policy has been trained with four clusters of material placed on the target location, we use a curriculum during training. We start by adding another cluster of material at the start of the rollouts. We also compute $t$ the farthest particle as $d_{part} (x^t_{far}) = \arg\max d_{part} (x^t_{mat})$. We then compute the distance between the tool position $x_{tool}$ and the farthest particle as $d_{tool} = ||x_{tool} - x^t_{far}||$. We compute $r_t = c_2 + w_1 (\Delta t d_{part} (x^t_{far})) + w_2 x_{plo} ||\Delta t x^t_{mat}|| + w_4 \Delta (d_{part} (x^t_{far}) < c_3)$, where $\Delta t$: denotes the difference of the quantities at timestep $t$ and $t + 1$. This reward term encourages moving particles to the goal. We also compute $t_{tool} = -w_3 d_{tool}$ that encourages the tool to move towards the farthest particle. The final reward defined below is chosen from the two terms based on a dynamically determined threshold $d_{thr} = \max(\frac{c_1}{d_{part} (x^t_{far})}, c_2)$.

$$r_t = \begin{cases} r_p & d_{tool} < d_{thr} \\ t_{tool} & \text{otherwise} \end{cases}$$  

To encourage gathering various number of clusters of materials to the target location, we use a curriculum during training. We start training the policy with a single cluster of material placed on the table. If a rollout during the training produces a total reward greater than a threshold, we advance the training to a new curriculum by adding another cluster of material at the start of the rollouts. We keep adding clusters until the policy has been trained with four clusters.

We trained two different gathering policies, one with granular material and another with visco-plastic material. The policy trained with granular material was unable to learn to gather more than a single pile. Training with visco-plastic material instead produced a policy that is able to sweep up four different material piles. Moreover, this same policy is also able to gather both granular and viscous fluid material.

### 4.2 Spreading

In the spreading task, we consider the opposite problem to the gathering task: we take an initially tight pile of material and we spread it evenly over the table’s surface. We show that a policy could spread visco-plastic materials in Figure 8 and spread granular materials in Figure 7.

In the material observation space $O_{mat}$, we provide both a density map and a height map for the material relative to the tool’s coordinate frame. For the tool state, $x_{tool}$ and $x_{tool}$ are each a 3D vector representing the position and velocity in all three dimensions. $r_{tool}$ and $t_{tool}$ are 2D vectors that represents the Euler angles and angular velocities about the vertical axis and the axis aligned with the bottom edge of the scraper. The action space contains the 3D position of the tool as well as its rotation around the axis orthogonal to the table surface. To enforce the scraper to push against the material during spreading, we tilt the scraper forward in the direction of its motion.

The reward function for the spreading task is designed as a combination of several terms: $r_t = w_1 r_m + w_2 r_{hc} + w_3 r_{th} + w_4 r_0$. The height count reward $r_{hc}$ measures the change in the number of occupied cells of the height maps of particles between two consecutive states:

$$r_{hc} = \text{sum}(\mathbb{1}(H_{t+1} > 0)) - \text{sum}(\mathbb{1}(H_t > 0)),$$

where $\mathbb{1}(H(x) > 0)$ counts the number of grid cells that has non-zero particle occupancy. The mean height reward $r_h$ measures the change in the average height of the material between two states:

$$r_h = \bar{y}_t - \bar{y}_{t+1}.$$
where $\bar{y}$ is the average height of all the particles. To encourage movement of particles above a certain height and penalized movement of particles on the table surface, we compute the particle movement reward $r_m$ as:

$$r_m = \frac{1}{n} \sum_{i=1}^{n} \left[ \frac{||x_{t+i}^i - x_t^i||}{||x_t^i - x_{t-1}^i||} \right]$$

where $c_{\min}$ is a constant threshold.

To avoid particles being pushed outside the edge of the table, we use a regularization term $r_o$ penalizing the outlier particles as:

$$r_o = -\sum_{i=1}^{p} \max(||\bar{x}_{\text{mat}}^i|| - c_{\text{rad}}, 0).$$

where $c_{\text{rad}}$ is the radius of the specified interior region.

Similar to the gathering task, we trained two different spreading policies, one using granular material and the other using visco-plastic material. Both policies can accomplish the spreading task successfully.

### 4.3 Flipping

In the third task, we demonstrate controlling a pan to toss and flip a disk of material in the air. See Figure 10 for a character that uses such a policy. The observation of the material for this task is a single image of the material height map relative to the tool. For the state of the tool, we observe the 3D position and velocity as well as the Euler angle and angular velocity around the horizontal axis. In addition to these, we have a 3D vector representing the angular velocity of the material that is observed by the policy. The action for the vector is a 4D vector with 3 translation and 1 rotation degree-of-freedom to control the position and tilting of the frying pan.

The reward function defined for this task is a combination of two terms as $r = w_0 r_h + w_{av} r_{av}$. By computing the minimum vertical distance of particles to the pan $d_{y_{\text{min}}} = \min_{i \in \{0,...,p\}} (y_i - y_{\text{tool}})$, the first term $r_h$ is defined as

$$r_h = \begin{cases} c_1 + w_1 d_{y_{\text{min}}} & d_{y_{\text{min}}} > 0 \\ w_2 d_{y_{\text{min}}} & \text{otherwise} \end{cases}$$

In addition to encouraging height, we also want to encourage the rotating motion of the material so that it can be flipped in the air. We compute the angular velocity vector of the material $\omega = \frac{1}{n} \sum_{i=1}^{n} \frac{(x_{\text{mat}}^i - x_t^i) \times \bar{x}^i}{||x_{\text{mat}}^i - x_t^i||}$, where $\bar{x}$ is the center-of-mass of all the particles, and $v_t^i$ is the velocity of the $i$th particle. We then define the angular velocity reward term as

$$r_{av} = \begin{cases} w_{\text{clip}} (\omega \cdot [1, 0, 0]^T, c_{\omega_{\text{min}}}, c_{\omega_{\text{max}}}) & d_{y_{\text{min}}} > c_2 \\ 0 & \text{otherwise} \end{cases}$$

Because we wanted the material being flipped to hold together, we used an elastic material for the disk. We can tune the reward function for this task to encourage flipping in either of two directions. We find that roughly half of the training runs for this task create successful outcomes that are reported in the reinforcement learning literature. We do not find this to be surprising, since there is substantial variation in the policy training outcomes that are reported in the reinforcement learning literature. All the constants and weights of all the experiments are included in Table 2.

### 4.4 Character Animation

To generate an animation of a character controlling the tool that manipulates the amorphous material, we use constrained optimization to solve a inverse kinematics (IK) problem. The desired solution of the IK is for the character to hold the tool and move it to track
the pose of the tool that is generated by the manipulation policy.
We solve:
\[
\begin{align*}
\min_{q_{\text{char}}'} ||q_{\text{char}}' - q_{\text{char}}|| \\
\text{subject to} \\
x_{\text{tool}}(q_{\text{char}}') = \hat{x}_{\text{tool}} \\
r_{\text{tool}}(q_{\text{char}}') = \hat{r}_{\text{tool}}, \\
C_{\text{joint}}(q_{\text{char}}') \geq 0
\end{align*}
\] (13)
where \(q_{\text{char}}'\) is the solution pose of the character in generalized coordinate, and \(q_{\text{char}}\) is the current character generalized coordinate, \(x_{\text{tool}}(q_{\text{char}}')\) and \(r_{\text{tool}}(q_{\text{char}}')\) are the position and orientation of the tool held by the character, and \(\hat{x}_{\text{tool}}\) and \(\hat{r}_{\text{tool}}\) are the target position and orientation of the tool generated from the manipulation policy. Lastly, \(C_{\text{joint}}(q_{\text{char}}')\) are the realistic joint limit constraints proposed in [Jiang and Liu 2018]. Results of a character controlling a tool to manipulate materials are shown in Figures 1, 9 and 10.

4.5 Comparing Observation Coordinate Frames
In this section we examine the importance of the coordinate frame of the image observations. In particular, we compare an absolute coordinate frame to a coordinate frame that is relative to the tool’s position and orientation. We compare the training results from both a spreading task and a gathering task on the visco-plastic material shown in Figure 12(a). Their respective learning curve shown in Figure 11 shows the performance difference over training.

For the spreading policy, relative observation also perform better than the absolute observations. This can be seen in Figure 12(b). The policy trained with relative observation is clearly able to spread the material in various directions, whereas the absolute observation trained policy is only able to spread the material along a single direction. With \(\sim 35M\) time steps, we can see from Figure 11 that the training using relative observation outperforms the absolute observation throughout the training.

4.6 Reward Ablation Study
Designing a good reward function is crucial to the success of our algorithm. In this section, we investigate the importance of different reward terms used in each of the tasks (gather, spread, flip) by training a policy with the reward term removed and comparing the performance of the ablated reward policy to the baseline policy with all reward terms.

4.6.1 Gathering. For the gathering task, we study the importance of the following four reward terms:

\[
(1) \, r_{\text{tool}} \text{ that encourages moving the tool to the farthest particle.} \\
(2) \, w_4 \sum_{p=0}^{P} ||\Delta t x_{\text{mat}}^p|| \text{ that encourages the movement of all particles.} \\
(3) \, w_4 \|d_{\text{part}}(x_{\text{far}}) < c_5\) \text{ that encourages particles to stay close to the vicinity of the goal.} \\
(4) \, w_1 (\Delta t d_{\text{part}}(x_{\text{far}})) \text{ that encourages moving the farthest particle towards the goal.}
\]

To compare the performance of each policy trained with different reward functions, we measure the farthest particle-to-goal distance across all particles at the last frame of the roll-out. We deploy each trained policy on 49 rollouts with different random initializations and report the average performance of each policy. A comparison of the ablated policies to the main result (all reward terms) is shown in Table 3. This study shows that the reward term (4) is most important to the success of the learning, and a policy will not be able to complete the task without this term. Removing the other reward terms (1-3) also results in negative impacts on the policy performances, demonstrating the usefulness of these terms.

Table 3. Comparison of gathering policies with ablated reward terms. Numerical evaluation is the farthest particle-to-goal distance. Smaller value means better performance of the policy.

|奖赏 | Full reward | (1) | (2) | (3) | (4) |
|---|---|---|---|---|---|
| | 0.66m | 1.69m | 1.25m | 1.56m | 6.63m |

4.6.2 Spreading. For the spreading task, we study how the absence of the following reward terms will affect the performance of a plastic material spreading policy.

Fig. 11. Comparison of relative and absolute observation for plastic gathering (left) and spreading (right) tasks. The three sharp drops of the red curve in the gathering task are when the curriculum has added another block of material.
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Fig. 12. Comparison of plastic material gathering and spreading. (a) shows the final state of a gathering policy using absolute observation and relative observation. (b) shows the similar states for the spreading policy.

(1) $r_m$ that encourages the movement of particles.
(2) $r_{hc}$ that encourages an increase in the number of occupied cells in the observed height map.
(3) $r_o$ that penalizes outlier particles that are pushed outside of the simulation region.
(4) $r_h$ that encourages a decreasing average height of the material.

We use the number of occupied cells of the height map that covers the table at the end of the rollout to evaluate the performance of a policy. The importance of each reward term is shown in Table 4. The results show that both reward term (2) and (4) are critical to the success of the policy training. Interestingly, reward term (4), which rewards the task completion indirectly by rewarding lower material height, turns out to be more important than reward term (2), which is directly related to the task being trained for. This is possibly because the reward term (2) is more sparse as it counts the number of occupied cells, which may not change between steps, while reward (4) is a more continuous measure that provides a smoother shaped reward signal. On the other hand, reward terms (1) and (3) are helpful for the training, but removing them does not prevent the policy from learning to solve the task.

Table 4. Comparison of spreading policies with ablated reward terms. Numerical evaluation is the mean number of occupied cells. Larger value means better performance.

| FULL REWARD | 336.12 |
|-------------|--------|
| (1) $r_m$   | 327.49 |
| (2) $r_{hc}$| 173.88 |
| (3) $r_o$   | 317.71 |
| (4) $r_h$   | 94.08 |

5 GENERALIZATION

We further study how a trained policy will generalize to materials simulated with higher resolution. We mainly focus on the generalization of policies on the gathering and spreading tasks for the visco-plastic material. For each of the policy trained on low resolution material (200 particles for the gathering task and 180 particles for the spreading task), we test it on a medium resolution and a high resolution material, where particle radius ratios are half and one-quarter compared to the training material particle size, respectively. For the gathering task, we used 1600 particles in the medium resolution material and 5400 particles in the high resolution material. For the spreading task, 1440 particles and 4860 particles are used in medium resolution material and high resolution material, respectively. Table 5 gives a comparison of using the trained policy on materials simulated with different resolution. The comparison uses the same metric described in 4.6. Figures 13, 14, 15, 16 show the initial and end frame of a rollout for both gathering and spreading tasks with higher resolution materials. For the gathering task, our policy is able to achieve good performance for the high resolution materials. We note that the drop in the measured performance for this task is partly due to the increased number of particles. For the spreading task, our policy can successfully generalize to the medium resolution material, while it failed in the high resolution material.

6 DISCUSSION AND LIMITATIONS

For the gathering task, policies trained using the plastic material performed significantly better than those trained on granular material. For this task, we speculate that chasing down loose particles (more common with the granular material) may adversely impact the training. Differences in training success when using different materials suggests the intriguing idea of using a curriculum of different material properties when training for some tasks.

Table 5. Comparison of policy on different simulation resolution

|           | LOW RES | MEDIUM RES | HIGH RES |
|-----------|---------|------------|----------|
| GATHERING | 1.06    | 2.49       | 2.77     |
| SPREADING | 336.12  | 391.90     | 96.04    |
Although we were able to train successful policies for the gathering, spreading and flipping tasks, there is still room for improvements. One common type of failure case we observe for the gathering task is that the scraper sometimes appears to hesitate before resuming pushing of the material. An example rollout of this is shown in Figure 17 where the scraper tries to reach the few particles on the upper left corner and fails to sweep them to the goal. This artifact might appear because the accurate position of the particles are not directly observed by the policy, introducing uncertainty to the policies behavior. For the spreading task, our policy does not achieve even spreading of the material to fully cover the entire table. Also, the materials are not guaranteed to stay connected afterwards. This could potentially be improved by using additional reward terms that encourage full coverage or connectedness of material during training. These properties would be important for reproducing many real-world tasks such as spreading paints.

Some of the limitations of our work are due to choices that we made in favor of faster policy training. The particle-based simulation in FleX is very efficient, yet is not able to model a large variety of materials. This leads us to the classic trade-off between better physical fidelity and higher computational cost. Simulators based on the Finite Element Methods (FEM) or the Material Point Methods (MPM) would provide more realistic simulations of visco-plastic materials or viscous fluid simulations. Unfortunately, these higher quality simulators come at a higher computational cost.

Despite the choice of an efficient simulator, simulating amorphous material is still computationally expensive. As such, we use relatively low simulation resolution of the materials during training. In our work, we demonstrate preliminary but encouraging results in generalization to higher resolution materials. Applying domain adaptation techniques could further improve the generalization and allow efficient policy training for more complex problems.

Another limitation of our current work is that we do not take into account the range of motion of the character when training the motion of a given tool. This means, for example, that a policy may be trained that rotates a hibachi scraper through 360 degrees or more while it gathers rice into a pile, which would require the character to re-grip the scraper. We could prevent this by taking into account the character’s range of arm and hand motion during the policy training. This would probably result in significantly higher training times, however.

Fig. 17. The scraper tries to reach the five particles but appears to hesitate before pushing them to the goal.

7 CONCLUSION

We have developed a learning-based system for creating characters that can manipulate amorphous materials using tools like a frying
pan or a scraper. We demonstrate that by designing suitable observation spaces, action spaces, and reward functions of the learning problem, we can obtain successful and generalizable control policies that achieve interesting manipulation tasks despite the high computation cost of simulating non-rigid objects. One of our key techniques is to have the agent observe the environment relative to the current pose of the tool, which leads to better learning performance and generalization capabilities of the policy. We test our algorithm on three manipulation tasks: gathering materials to a certain position on the table, spreading the material evenly, and pan-flipping. We collectively show our system on multiple types of materials such as uncooked rice (granular), meat patty (plastic), and egg whites (viscous fluid).

In this work, we investigated manipulation tasks that involve relatively simple forms of tool usage: holding a pan or a scraper, while humans can perform more sophisticated and intricate manipulation task with amorphous materials, such as making dumplings or peeling fruit. Many of these tasks involve dexterous manipulation, which notably increases the dimension and complexity of the action space. An interesting direction for future work is thus to expand our current learning system to handle these more challenging manipulation tasks. Another future direction is to include a more diverse set of materials with higher physical fidelity. To combat the potential additional cost in simulating these materials, one promising approach would be to use curriculum learning, where we train the policy with increasingly complicated materials throughout the learning. How to effectively choose the sequence of materials to form the curriculum in order to minimize the total training time would be an intriguing research problem.

ACKNOWLEDGMENTS
We thank Alexander Clegg, Henry Clever, Zackory Erickson and Yifeng Jiang for discussions and technical assistance. This work is supported by NSF award IIS-1514258.

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