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Kanas, Nikola; Bjørk, Rasmus; Wells, Kristin Høydalsvik; Schuler, Raphael; Einarsrud, Mari Ann; Pryds, Nini; Wiik, Kjell

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Time-Enhanced Performance of Oxide Thermoelectric Modules Based on a Hybrid p–n Junction

Nikola Kanas, * Rasmus Bjørk, Kristin Høydalsvik Wells, Raphael Schuler, Mari-Ann Einarsrud, Nini Pryds, and Kjell Wiik

ABSTRACT: The present challenge with all-oxide thermoelectric modules is their poor durability at high temperatures caused by the instability of the metal-oxide interfaces at the hot side. This work explains a new module concept based on a hybrid p–n junction, fabricated in one step by spark plasma co-sintering of Ca3Co4−δOδ+6 (CCO, p-type) and CaMnO3−δ/CaMn2O4 (CMO, n-type). Different module (unicouple) designs were studied to obtain a thorough understanding of the role of the in situ formed hybrid p–n junction of Ca3CoMnO6 (CCMO, p-type) and Co-oxide rich phases (p-type) at the p–n junction (>700 °C) in the module performance. A time-enhanced performance of the modules attributed to this p–n junction formation was observed due to the unique electrical properties of the hybrid p–n junction being sufficiently conductive at high temperatures (>700 °C) and nonconductive at moderate and low temperatures. The alteration of module design resulted in a variation of the power density from 12.4 (3.1) to 28.9 mW/cm2 (7.2 mW) at 197 °C due to 2 days of isothermal hold (900 °C hot side). This new concept provides a facile method for the fabrication of easily processable, cheap, and high-performance high-temperature modules.

1. INTRODUCTION

Waste heat released during high-temperature processes (e.g., in the metallurgical industry) is significant with respect to cost and energy-effective production.1 Thermoelectric generators (TEGs) convert heat directly into electrical energy, thus representing promising technology for waste heat harvesting. The materials which constitute these devices are often toxic and expensive metals and alloys,2,3 and their use is also hampered by severe limitations due to oxidation and low melting temperatures. This paves the way for oxide-based TEGs, which provide chemical and thermal stability at high temperatures, and in addition are low-cost and environmentally friendly.4 To date, the electrical output power of oxide-based TEGs is generally lower than that of the state-of-the-art TEGs.5 However, the output power is not always the key parameter to evaluate TE modules. For instance, TE modules, which generate a moderate electric power and possess good durability, are recognized as potential power sources for wireless sensors that could continuously operate at elevated temperatures.6

Currently, the main strategies to improve the efficiency of oxide-based TE modules for waste heat harvesting are improving the doping of the individual p- and n-type materials to enhance their performance,7 reducing the contact resistance,8,9 and including barrier layers to reduce diffusion.10

A notable improvement was achieved with “leg-segmented modules”11–13; however, oxide-based modules still suffer from poor durability caused by the instability of the metal-oxide interfaces at the hot side.12,14 Hence, there is a demand for new approaches and strategies to improve the performance of oxide-based modules in terms of long operation time under a high-temperature gradient.

Ca3Co4−δOδ+6 (CCO) is one of the most promising oxide thermoelectric p-type materials for high-temperature applications.15–17 It has a misfit layered structure consisting of two sublattices: a rock salt Ca3CoO3 and a CdI2-type CoO2.15,16 The two sublattices have different b parameters, which results in an incommensurable crystal structure. The application of CCO in air is limited to temperatures below 930 °C due to decomposition.17

CaMnO3−δ is a promising thermoelectric n-type material with a perovskite structure.18 At 900 °C in air, the cubic phase is stable, changing to tetragonal and orthorhombic phases with

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decreasing temperature.\textsuperscript{19} It has recently been shown that CaMnO$_{3-\delta}$-based composites (CMO), composed of CaMnO$_{3-\delta}$ as the major phase and CaMnO$_{4}$ as the minor phase, demonstrated better TE performance than pristine CaMnO$_{3-\delta}$ due to enhanced electrical conductivity.\textsuperscript{20} Hence, this material is selected as the n-type material in this work.

At high temperatures, CCO and CMO react to form Ca$_{3}$CoMnO$_{6}$ (CCMO). CCMO crystallizes in the $\text{AB}_{2}$BO$_{6}$ structure, consisting of alternating face-sharing CoO$_{6}$ octahedra and trigonal bipyramidal chains, with Ca ions between the chains.\textsuperscript{11,12,21} Electrical conductivity increases exponentially above 800 °C due to the pronounced polaron hopping mechanism, reaching a maximum of 10$^{-4}$ S cm$^{-1}$ at 900 °C, followed by a high positive Seebeck coefficient.\textsuperscript{23} High-temperature stability of Ca$_{3}$CO$_{2-x}$Mn$_{x}$O$_{6}$ for 1 < x < 0.75 has been reported.\textsuperscript{24}

In our recent publication, a prototype TE module consisting of p-type CCO and n-type CMO with a p–n–p junction (CCO/CMO/CCO) demonstrated promising performance (≈23 mW cm$^{-2}$) attributed to the formation of the non-rectifying p–p–n junction and unexpectedly high open-circuit voltage. In this work, parts of the legs were separated by LaAlO$_{3}$ (LAO), which is an electrical insulator, while direct contact between CMO and CCO was established at the high-temperature end.\textsuperscript{25} The origin of the enhanced performance is only partially understood and was attributed to CCMO formation at the p–n junction on the hot side of the module.

Later, a detailed transmission electron microscopy (TEM) study of the CCO–CMO interface showed that both the CCMO and Co-oxide phases formed at 900 °C, and the interdiffusion and phase distribution were more accurately described.\textsuperscript{26} However, the understanding of how the module design, including the hybrid p–n junction, affects the performance is lacking.

In the present study, we use the novel concept of a hybrid p–n–p junction and analyze the performances of modules with various different designs to elaborate on the impact of the formation of the reaction layers. Our hypothesis based on previous work is that the formation of CCMO and Co-oxide will establish sufficient electrical contact and conductivity at high temperatures (hybrid p–n junction), and act as an electrical insulator at medium and low temperatures due to the low electrical conductivities of both the phases. A comprehensive understanding of the time-enhanced performance of oxide modules based on the hybrid p–n junction is provided in addition to a discussion on future module design.

2. RESULTS

Figure 1 shows a schematic illustration of the four different modules investigated. The aim of different designs was to obtain a more thorough understanding of the role of the hybrid p–n junction with respect to the module performance.

Figure 2a shows the thermoelectric performance of Module1-0h with 700, 800, and 900 °C hot side temperatures, corresponding to $\Delta T$ of 512, 606, and 652 °C, respectively. The properties, $V_{oc}$, $I_{sc}$, and $P_{max}$ of Module1-0h are enhanced with increasing hot side temperature, reaching maximum values of 207 mV, 50 mA, and 2.7 mW at 900 °C ($\Delta T = 652$ °C), respectively. Performance of Module1-0h, as a function of time at the maximum hot side temperature (900 °C) is shown in Figure 2b.

Time-enhanced performance of the Module1-0h is observed corresponding to 11, 14, and 14.5% increase in $V_{oc}$, $I_{sc}$, and $P_{max}$, respectively.
Seebeck coefficients for CCO and CMO materials reported by Kanas et al., and as expected, $V_{oc}$ increases with $\Delta T$. The experimental values obtained for $V_{oc}$ (Table 1) are included in Figure 4 (diamonds) and are significantly higher than $V_{oc}$ resulting from COMSOL modeling. It is interesting to note that the difference between calculated and measured open-circuit voltages ($\Delta V_{oc}$) decreases with increasing degree of separation between the n- and p-type materials. The highest $V_{oc}$ modeled are for a module where the p- and n-legs are separated and connected by a metallic interconnect at the high-temperature side of the module, i.e., a conventional device, which is not realized experimentally in the present work. To obtain full matching of experimental and theoretical data in the whole range of separations, the modeling should also include the contribution from the hybrid p–n junction.

After the assessment of the performance of Module1-0h, the microstructure was analyzed by scanning electron microscopy (SEM) on cross-sections at the hot and cold side of the module (Figure 5). Microstructures in the vicinity of the p–n interface exposed to $\sim 250^\circ$C (Figure 5d–f) were significantly different from those exposed to $\sim 900^\circ$C (Figure 5a–c). Pronounced grain growth and increase in pore size were observed at the hot side of the module, along with the formation of CCMO and Co-oxide enriched layers at and in the vicinity of the interface, which is in accordance with our previous study. Both in situ formed layers are much denser than the surrounding matrix, and the “gap” along the p–n junction is due to the material being pulled out during polishing. The transition point from unreacted (Figure 5e) to reacted p–n junction (Figure 5b) was determined by SEM to be about 25% of the total height (bottom up). This is also illustrated in Figure 1 (Module1-0h).

The microstructural changes in the p- and n-type materials along the entire height are the same in all modules, due to the same geometry of the modules and the same thermal gradient applied. Hence, there are no significant differences in the material properties among the modules, and hence the observed $V_{oc}$ discrepancy is attributed to the different areas left for the formation of the hybrid p–n junction.

The reactions between CCO and CMO were studied separately, and Figure 6a,b shows the time dependency of the thicknesses of the in situ formed CCMO and Co-oxide layers as a function of isothermal heat treatment (1, 3, 6, 12, 24, and 48 h) at 900 and 700 °C, respectively. At both temperatures, the thicknesses of the Co-oxide layers are significantly larger than those of CCMO. The Co-oxide layer achieves a thickness of about 20 μm after 50 h dwell time at both 700 and 900 °C, whereas CCMO layers were of 0.5 and 2 μm, respectively. The influence of the formed layers on the electrical properties was further investigated, and the resistance ($\Omega \cdot \text{cm}^{-2}$) across the as-sintered CMO–CCO pellets was continuously monitored for 70 h at 700, 800, and 900 °C (Figure 6c). There is a significant
decrease in resistance with increasing temperature and the resistance at 700 and 800 °C shows a moderate decrease with time, and the opposite trend is observed at 900 °C. This is probably related to the increasing thickness of the dense CCMO layer at 900 °C (Figure 6a) since the Co-oxide layer is formed as separate grains (not a continuous barrier) and as such does not affect the resistance that much. However, the main voltage drop occurs over the junction, and the resistivity of active components does not contribute. The resistance contribution of CCO and CMO at 700, 800, and 900 °C is given in Table S1 and compared to the resistance of the junction (Supporting Data).

High-temperature X-ray diffraction (HT-XRD) patterns of homogeneously mixed CCO–CMO powders are presented in Figure 7. The presence of both CMO and CCO is evident at room temperature, and the intensity of the CCO diffraction peaks increases with temperature due to increasing crystallinity. At 714 °C, the diffraction lines of CCMO and Co3O4 appear, and the intensity of these diffraction lines is increasing with increasing temperature. At 779 °C, CoO becomes the stable phase due to the reduction of Co3O4.17,30

3. DISCUSSION

3.1. Time-Enhanced Performance due to In Situ Reaction. Figure 8 shows an overview of the monotinous increase in $P_{\text{max}}$ of the modules investigated (Figures 2 and 3). A reaction layer between the n- and p-materials is developed during high-temperature testing followed by a significant decrease in thickness from the hot to the cold end (Module1-0h) when $\Delta T$ is applied (sketched in Figure 1). The absence of the reaction layer at medium and low temperatures (25% of height $\sim 2.7$ mm) corresponds to a significant degree of short-circuiting ($\sim 40\%$) between the p- and n-legs resulting in low
power output. Although Module1-0h shows the lowest performance (Figure 8a), a significant increase in performance is observed with time (Figure 8b) due to the beneficial reactions taking place at the high-temperature end of the device. Inner resistance of the modules (R) decreases as temperature increases due to a combination of reduced resistance with temperature (Figure 6c) and consolidation of electrical contact at the high-temperature end of the module with time (sintering). Figure 8a shows a significant difference in R between Module1-24h (2.5 Ω) and Module2-75%LAO (>4 Ω), which is due to the pre-sintering of Module1-24h at 900 °C for 24 h prior to testing and establishing an enhanced electrical contact between the legs. The higher resistance observed for Module2-75%LAO is due to the absence of the pretreatment; this module was tested as received from spark plasma sintering (SPS). However, Figure 8a shows a significant decrease in R with time for Module2-75%LAO, corresponding to a continuous improvement in the electrical contact between the legs at the high-temperature end of the module. There is no clear trend between R and V_{oc} (Figures 2, 3, and 8a), and the reason may be because R is measured while a current passes through the module and V_{oc} is the potential at open-circuit (zero current).

Module1-24h with a uniform thickness of the hybrid p–n junction prior to the test, resulted in moderate time-enhanced performance (Figure 8). However, P_{max} is much higher than that of Module1-0h, even after 42 h of isothermal testing (Figure 8). These observations support our assumption that the reaction layer can work as an electrical insulating material at moderate and low temperatures, reducing the degree of short-circuiting and enhancing the power output.

An electrical insulator (LAO) was applied in the Module2-series (Figure 1), and a time-enhanced performance (Figures 3b,d and 8) was observed. The performance of Module2-25% LAO is lower than that of Module1-24h, likely due to the absence of a reaction layer along the mid-parts of the interface between the n- and p-legs, reducing the power due to short-circuiting. However, extending the electrical insulating layer (LAO) to 75% of the total length results in a significant enhancement in performance. Module2-75% shows the highest P_{max} among all modules tested and shows the effect of separating the legs electrically and suppressing the extent of short-circuiting. Module2-75% also demonstrates a time-enhanced performance interpreted as an improved electrical contact between the legs with time at the hot end of the device. These observations are supported by the COMSOL modeling presented in Figure 4. The modeling is based on the contact between various parts of the legs, ranging from contact between the legs over the full length (0% separation) to contact only at the high-temperature end of the module (metallic interconnect). The measured V_{oc} for all modules is enhanced compared to modeled values and confirms the beneficial effect of the phases formed at the interface between the legs.

However, as opposed to Module2-25% (Figure 3b), V_{oc} of Module2-75% decreases with time (Figure 3d). Because the V_{oc} is proportional to the Seebeck coefficient and temperature gradient, the observed reduction is somewhat surprising and not easily explained. However, it might be a side-effect related to thermal excitation and separation of bipolar charge carriers from the space charge region (by a built-in field),\textsuperscript{31,32} since the thermopower drop could be caused by an increase in charge carrier concentration in both the active components.\textsuperscript{31,32}

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Figure 4. Calculated (COMSOL) open-circuit voltages (V_{oc}) as a function of ΔT for modules with different cell design. A dotted vertical line represents experimental cold side temperature during the module characterization at the 900 °C hot side. Three V_{oc} values measured at 900 °C hot side of Module1-0h (black diamond solid), Module2-25%LAO (red diamond solid), and Module2-75%LAO (blue diamond solid) were taken from Table 1 for comparison.
Although Module2-75% shows the benefit of inserting an electrical insulating material (LAO) between the legs, the Module1 series holds great promise for future manufacturing of oxide-based devices based on CMO and CCO. The significant decrease in the resistivity of the reaction layer with temperature (Figure 6) shows that co-sintering of CMO and CCO is a promising approach to simplify the production of stable modules, which can operate at high temperatures in air. Our investigation also shows that there are ample opportunities to enhance the performance further by even more accurate control of the variation in thickness of the reaction layer along the interface between CMO and CCO. This study is also encouraging with respect to high-temperature and long-term operation of the modules. In conclusion, our approach enables “smart engineering” through simple design, easy fabrication, and good performance.

4. CONCLUSIONS

The influence of the high-temperature reaction at the p–n junction and the cell design alteration on the performance of CMO–CCO-based modules were analyzed. The interfacial reaction occurs above 700 °C and results in the formation of a hybrid p–n junction (CCO/CMO/Co-oxide/CMO), demonstrating a time-enhanced performance. Unique electrical properties of the hybrid p–n junction were utilized to manufacture a module with a conductive top and non-conductive bottom side, and the reaction layer was an electrical insulating material at moderate and low temperatures. The maximum increase in $P_{\text{max}}$ over 2 days was realized by Module2-25%LAO, corresponding to a 21% increase, while the highest $P_{\text{max}}$ of 7.2 $\mu$W ($\sim$29 mW/cm²) was generated by Module2-75%LAO. The present work provides a novel platform for designing a range of interface-based modules stable at high temperatures under an ambient atmosphere.

5. EXPERIMENTAL SECTION

5.1. Processing. Powders of the p-type $\text{Ca}_3\text{Co}_{4-x}\text{O}_{9+\delta}$ (CCO), electrical insulating LaAlO$_3$ (LAO), and n-type $\text{CaMnO}_3-\delta$/$\text{CaMn}_2\text{O}_4$ composite (CMO) were synthesized by spray pyrolysis (CerPoTech AS, Trondheim, Norway). Two series of modules with different designs were constructed: (i) co-sintered large-area p–n junction (Module1) and (ii) co-sintered p–n junction together with LAO tape placed between the p- and n-type materials (Module2). LAO tapes were prepared by tape casting followed by lamination and cutting, with the purpose of partially separating the active components in the module. The length of the LAO tapes was such that 25 and 75% of the height of the module was separated by the LAO layer (3.3 and 8.8 mm, respectively); hence the samples were referred to as Module2-25%LAO and Module2-75%LAO. Binder removal from tapes is described elsewhere.$^{25}$ The thermoelectric performance of Module1-0h was characterized as received from the spark plasma sintering (SPS, Dr Sinter 825, Saitama, Japan), while Module1-24h was heat-treated at 900 °C for 24 h prior to the assessment of the performance. The performance of the Module2 samples was also characterized as received from SPS. The preparation of Module1-0h and Module1-24h was based on filling of the
Figure 8. (a) Overview of \( P_{\text{max}} \) (spheres) and inner resistance, \( R \) (solid lines) of different modules exposed to 900 °C hot and 250 °C cold side as a function of time, and (b) a histogram indicates the percentage of time-enhancement during the isothermal test.

graphite dies (12 mm) with CMO and CCO powders according to ref 25. In the case of Module2-25%LAO and Module2-75%LAO, an electrically insulating LAO tape was placed on the CMO powder before CCO powder was poured into the die. All four modules were fabricated by spark plasma co-sintering in a vacuum at 860 °C for 3 min and 75 MPa, at 160 K/min heating rate. A small area of about 0.6 mm from the top and the bottom of the co-sintered pellets were removed by grinding/polishing to ensure vertical free-standing modules (~10.7 mm height) and low thermal contact resistance. The final thicknesses of CCO and CMO in the modules were ~0.9 and 3.5 mm, respectively.

The same sintering conditions and geometry as those used for module fabrication were used for the preparation of 13 as-sintered CCO–CMO junctions, three for \textit{in situ} isothermal \( I–V \) measurements, and 10 for SEM/energy-dispersive X-ray spectroscopy (EDS) analysis to understand the growth of the \textit{in situ} formed layers at different temperatures.

\( \text{Ca}_3\text{Co}_{5−x}\text{O}_{9+δ} \) (CCO) and \( \text{n-type } \text{CaMnO}_{3−α}/\text{CaMn}_2\text{O}_4 \) (CMO) powder mixture (CCO–CMO mixture) was prepared by hand mixing in a mortar, followed by mixing in isopropanol using a magnetic stirrer.

5.2. Characterization. The disk-shaped modules with small flat regions at the top and bottom were placed vertically on an alumina plate. CCO and CMO were brought in contact with Pt-wires at the cold side using a commercial silver paste. Modules with Pt-wires embedded in silver paste were heated at 280 °C for 2 h in ambient air, to obtain sufficient electrical contact between the Pt-wires and the active components. The characterization of the modules was performed in ambient air, via variation of the load resistance at 700, 800, and 900 °C, corresponding to thermal gradients (\( \Delta T \)) of 512, 606, and 652 °C, respectively. The \( \Delta T \)s were established by heating the hot side of the module using a Joule heater, while the cold side was cooled using a watercooler. The temperature measurements were carried out using two S-type thermocouples. A voltmeter was connected in parallel to the ampere meter, variable resistor (in series to each other), and to the module. Current–voltage curves were recorded during automatic switching of load resistance, when thermal equilibria were established at each temperature. After the characterization at 700, 800, and 900 °C, respectively, all modules were exposed to isothermal tests at 900 °C (\( \Delta T \sim 652 ^{\circ} \)) where the open-circuit voltage (\( V_{\text{oc}} \)), short-circuit current (\( I_{\text{sc}} \)), and electrical power output (\( P_{\text{max}} \)) were recorded at given times.

After characterization, Module1-0h was polished with a diamond paste (DiaPro NapB1) to 1 µm smoothness and coated with carbon (Cressington Carbon Coater 208, Watford, U.K.) for microstructural characterization by SEM (Hitachi S-3400N, Tokyo, Japan).

Three as-sintered CCO–CMO samples with identical geometry as Module1-0h were horizontally placed in a ProboStat cell (NORECS, Oslo, Norway) for isothermal characterization by current–voltage measurements at 700, 800, and 900 °C for 72 h using a Gamry Reference 3000 Potentiostat.

\textit{In situ} high-temperature X-ray diffraction (HT-XRD) measurements on the dried CCO–CMO powder mixture were performed up to 779 °C with steps of 22 °C. The powder mixture was placed into an alumina sample holder mounted into a Bruker D8 Advance diffractometer (Karlsruhe, Germany) with a Cu Kα source and VANTEC Superspeed detector and heated with a radiant heater. The rate of heating was 0.1 °C·s⁻¹. The temperature was calibrated by refining the lattice parameters of \( \alpha_2\text{O}_3 \) powder as a function of temperature. The 2θ range of 10−75° was scanned with a step size of 0.025° with 4 s per step, giving a total collection time of about 3 h per scan. Each scan was delayed by 30 min to ensure that the sample had equilibrated at the set temperature.

The fabricated modules were modeled using a finite element framework COMSOL Multiphysics, in which the coupled differential equations describe the electrical current density and the heat flux, as given in refs 33, 34. We modeled a 2D cross-section of the modules where a heat loss to the surroundings was not considered. Material properties for the modeled materials were taken from Kanas et al.25 The model was used primarily to calculate the open-circuit voltage (\( V_{\text{oc}} \)) for the various alternative cell designs, as this parameter does not depend on any electrical resistance of the interfaces between electrodes and active components, and could thus directly be
compared to experimental values. The $V_{oc}$ was calculated as a function of the temperature gradient within the module with different p–n areas.

### ASSOCIATED CONTENT

#### Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acsomega.0c04134.

Details about calculated resistances of the individual p- and n-type materials together with the total resistance of the hybrid p–n junction developed at 700, 800, and 900 °C (PDF)

### AUTHOR INFORMATION

#### Corresponding Author

Nikola Kanas — Department of Materials Science and Engineering, Norwegian University of Science and Technology (NTNU), 7491 Trondheim, Norway; Department of Energy Conversion and Storage, Technical University of Denmark, 2800 Kongens Lyngby, Denmark; orcid.org/0000-0001-7906-7862; Email: nikola.kanas@ntnu.no

#### Authors

Rasmus Bjørk — Department of Energy Conversion and Storage, Technical University of Denmark, 2800 Kongens Lyngby, Denmark

Kristin Hoydalsvik Wells — Department of Materials Science and Engineering, Norwegian University of Science and Technology (NTNU), 7491 Trondheim, Norway

Raphael Schuler — Department of Chemistry, University of Oslo, FERMI0, 0349 Oslo, Norway

Mari-Ann Einarsrud — Department of Materials Science and Engineering, Norwegian University of Science and Technology (NTNU), 7491 Trondheim, Norway; orcid.org/0000-0002-3017-1156

Nini Pryds — Department of Energy Conversion and Storage, Technical University of Denmark, 2800 Kongens Lyngby, Denmark; orcid.org/0000-0002-5718-7924

Kjell Wiik — Department of Materials Science and Engineering, Norwegian University of Science and Technology (NTNU), 7491 Trondheim, Norway

Complete contact information is available at: https://pubs.acs.org/10.1021/acsomega.0c04134

#### Notes

The authors declare no competing financial interest.

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