A systems biology study on NFκB signaling in primary mouse hepatocytes

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The cytokine tumor necrosis factor-alpha (TNFα) is one of the key factors during the priming phase of liver regeneration as well as in hepatocarcinogenesis. TNFα activates the nuclear factor κ-light-chain-enhancer of activated B cells (NFκB) signaling pathway and contributes to the conversion of quiescent hepatocytes to activated hepatocytes that are able to proliferate in response to growth factor stimulation. Different mathematical models have been previously established for TNFα/NFκB signaling in the context of tumor cells. Combining these mathematical models with time-resolved measurements of expression and phosphorylation of TNFα/NFκB pathway constituents in primary mouse hepatocytes revealed that an additional phosphorylation step of the NFκB isoform p65 has to be considered in the mathematical model in order to sufficiently describe the dynamics of pathway activation in the primary cells. Also, we addressed the role of basal protein turnover by experimentally measuring the degradation rate of pivotal players in the absence of TNFα and including this information in the model. To elucidate the impact of variations in the protein degradation rates on TNFα/NFκB signaling on the overall dynamic behavior we used global sensitivity analysis that accounts for parameter uncertainties and showed that degradation and translation of p65 had a major impact on the amplitude and the integral of p65 phosphorylation. Finally, our mathematical model of TNFα/NFκB signaling was able to predict the time-course of the complex formation of p65 and of the inhibitor of NFκB (IκB) in primary mouse hepatocytes, which was experimentally verified. Hence, we here present a mathematical model for TNFα/NFκB signaling in primary mouse hepatocytes that provides an important basis to quantitatively disentangle the complex interplay of multiple factors in liver regeneration and tumorigenesis.

Keywords: mathematical modeling, p65, IκB, protein degradation, hepatocytes, signaling

1. INTRODUCTION
Liver regeneration after tissue damage is a tightly regulated spatio-temporal process, which is primarily controlled by specific growth factors and cytokines (Michalopoulos, 2010). It predominantly relies on the fast initiation of hepatocyte proliferation after injury and only few proliferative cycles are necessary to restore the liver mass and function (Papp et al., 2009).

Tumor necrosis factor-alpha (TNFα), which is predominantly secreted from liver-resident macrophages (Kupffer cells), represents one of the earliest stimuli for proper initiation of hepatocytic proliferation (Yamada et al., 1997). The most extensively characterized response activated by TNFα is the highly conserved nuclear factor of κ-light-chain enhancer of activated B cells (NFκB) pathway, which can initiate hepatocytic mitotic cycles after entering the nucleus. After partial hepatectomy (PHx), which is the best experimental model for studying liver regeneration, the level of TNFα increases dramatically within 1 h, leading to fast activation of NFκB signaling (Diehl and Rai, 1996). The pivotal relevance of TNFα-induced signaling is supported by the fact that in type I TNFα receptor-deficient mice, hepatocyte proliferation is strongly reduced and liver regeneration is impaired after PHx (Yamada et al., 1997).

Activation of the NFκB axis involves the formation of homo- or hetero-dimeric transcription factors composed of different subunits: p50 (NFκB1), p52 (NFκB2), p65 (RelA), RelB, and c-Rel (Hayden and Ghosh, 2012). In absence of pathway activation, these dimers are disabled by a family of inhibitory proteins including IκBα, IκBβ, IκBγ, and IκBε. For example, binding of IκBα to hetero-dimeric p65:p50 results in steady-state cytoplasmic complex retention and therefore prevents dimers from binding their respective DNA recognition sites. Upon TNFα stimulation, different regulatory proteins are recruited in close proximity to the TNFα receptor and form the receptor-associated signalingosome. Subsequently, IκBα phosphorylation is mediated by a kinase
complex composed of IkB kinase-α (IKKα), IkB kinase-β (IKKβ), and IkB kinase-γ (IKKγ or NEMO), followed by proteasomal degradation of inhibitory IkBα as well as release and nuclear translocation of p65/p50 complexes. These nuclear heterodimers induce transcription of genes involved in the initiation of proliferation as well as negative regulation of apoptosis (Hayden and Ghosh, 2012).

The modulation of NFκB signaling results in different expression signatures in vivo and in vitro (Ashall et al., 2009; Li et al., 2009; Sung et al., 2009). This could be achieved by posttranslational modifications such as alternative phosphorylation of the involved signaling components. Multiple phosphorylation sites have been described for the NFκB subunit p65 (Viator et al., 2005). Most common is the phosphorylation of p65 at serine 536 that is mediated by IKK-β, Akt, and RSK1 in response to TNFα (Sakurai et al., 1999), and IL1β (Madrid et al., 2001) stimulation and DNA damage (Bohuslav et al., 2004). Other phosphorylation sites and kinases are gaining importance for regulating p65 transcriptional activity.

The protein kinase C, zeta (PKCζ) is capable to phosphorylate free p65 at serine 311 when translocated into the nucleus following TNFα stimulation (Durán et al., 2003). Furthermore another specific p65 phospho-site, serine 276, has been shown to be a target for protein kinase A, c (PKAc), and mitogen-activated protein kinase 14 (MAPK14/MSK1; Vermeulen et al., 2003; Jamaluddin et al., 2007). These kinases are of particular interest since they are localized in the nucleus and provide the possibility to modify the transcriptional activity of p65 that translocates to the nucleus subsequent to phosphorylation at serine 536 by IKK-β. However, currently there is not much known about their direct involvement in the regulation of canonical NFκB signaling (Joo and Jetten, 2008) and the efficiency of antibodies used for detection are controversially discussed (Spooren et al., 2010).

Another important feature of NFκB signaling is ligand-independent, basal, and ligand-dependent turnover of the signaling components. Basal degradation of IkBα has been reported (Krappmann et al., 1996; Pando and Verma, 2000) suggesting that two different IkBα pools, p65-bound and free unbound, exist. In both cases, IKK-β-mediated IkBα phosphorylation was not necessary for basal protein degradation. However, the pool of free IkBα represents only 15% of the total protein amount (Rice, 1993) and thus specific mechanisms are required to explain basal degradation of free and p65-bound IkBα (Mathes et al., 2008). Combining genetic tools and mathematical models Mathes et al showed that free IkBα degradation is independent of its phosphorylation or ubiquitination but mainly mediated by a specific C-terminal sequence (PEST) able to fine-tune turnover of free IkBα protein. On the other hand, different from the rather instable free IkBα, p65 is relatively stable and upon complex formation with IkBα protects IkBα from fast degradation. IKK-β-mediated phosphorylation of p65-bound IkBα in response to TNFα stimulation leads to the release of the complex unmasking the PEST sequence and results in an efficient recognition and fast degradation by the proteasome. Thus, basal and ligand-dependent turnover operate on different time scales. Their specific contribution to signal amplitude and duration remains to be elucidated.

In the past, the dynamic behavior of NFκB has been intensively analyzed in different cancer cells and immortalized fibroblasts (Cheong et al., 2006; Ashall et al., 2009). Particularly, time-resolved phosphorylation analysis of pathway constituents (including p65 and IkBα) followed by the activation of target genes involved in feedback regulation (e.g., IkBα, A20) leads to the identification of sustained oscillatory behavior in NFκB signaling (Nelson et al., 2004).

In this regard, NFκB signaling has been extensively studied by computational modeling. Carlotti et al. (1999, 2000) presented a first computational study focused on the investigation of the NFκB shuttling, whereas Hoffmann et al. (2002) studied the whole signaling module. The model by Nelson et al. (2004) pointed to the importance of the IkBα transcription rate for the frequency of oscillations and further analysis suggested IkBα and A20 have a major impact on the pathway dynamics (Werner et al., 2008). Another study reported a key role for IkBα and IKKs in oscillations and protein turnover (Ihekwaba et al., 2004; Cheong et al., 2006). Recently, the influence of model parameters on the pathway dynamics has been studied identifying NFκB concentration to be the most decisive parameter for oscillations (Wang et al., 2011).

Only few studies included protein synthesis and degradation rates as relevant parameters for NFκB signaling dynamics (O’Dea et al., 2007). In some cases, IkB turnover is part of the model, but NFκB, e.g., p65 turnover has not been included so far, which is probably due to the relatively stable levels of NFκB. However, it is problematic to predict the influence of stable proteins on systems behavior. O’Dea et al. (2007) measured and modeled the influence of NFκB binding on the degradation rate of IkBα species, which was important for their computational predictions. Thus, NFκB seems to protect IkB species from unstimulated degradation. None of the described studies analyzed and modeled NFκB signaling in primary and non-malignantly transformed hepatocytes representing the major cell population of the liver involved in regeneration and tumorigenesis.

Here we present a hepatocyte-specific model for TNFα-induced NFκB signaling that considers basal protein turnover and facilitates the prediction of TNFα-induced complex formation of p65 and IkBα. Since not all parameters of the model are fully identifiable we study an ensemble of 30 different parameter sets that each fit our experimental data. Model validation and conclusions are based on common properties of the ensemble of models.

2. MATERIALS AND METHODS

2.1. EXPERIMENTAL: ANIMAL WORK, ISOLATION OF PRIMARY MURINE HEPATOCYTES, AND CULTURE CONDITIONS

C57Bl/6 mice were obtained from Charles River (Wilmington, MA, USA) and housed under standard conditions in the DKFZ animal facility. All experiments were performed with the approval of the German Regional Council of Baden-Wuerttemberg (Karlsruhe, Germany) and in accordance with the institutional regulations. Isolation of hepatocytes from mice has previously been described (Castoldi et al., 2011). In brief, six to twelve weeks old animals were anesthetized using 10% ketamine hydrochloride (5/100 mg body weight) and 2% xylazine hydrochloride (1/100 mg body weight), and perfused with HANKS solution supplemented with 0.3 mg/ml weight) and 2% xylazine hydrochloride (1/100 mg body weight), and perfused with HANKS solution supplemented with 0.3 mg/ml.
collagenase CLSII and 5 mM CaCl$_2$. After liver removal, hepatocytes were plated on collagen-coated culture dishes (1 million cells/6 cm BD; Biocoat; Horsham, PA, USA) and cultured with adhesion medium (Williams' medium E (Biochorn, Berlin, Germany), 10% FCS, 0.1% insulin, 100 nM dexamethasone, 2 mM l-glutamine, and 1% penicillin/streptomycin) at 37°C for 4 h. After attachment, cells were washed with PBS (GIBCO Life Technologies, Darmstadt, Germany) and incubated over-night with pre-starvation medium (Williams’ medium E, 100 nM dexamethasone, 2 mM l-glutamine, and 1% penicillin/streptomycin). Before TNFα stimulation, cells were incubated in starvation medium (Williams medium E and 1% penicillin/streptomycin) for 5 h. Dynamic simulation of NFκB signaling was achieved by administration of recombinant murine TNFα (10 ng/ml; R&D Systems, Minneapolis, MN, USA) in starvation medium. At different time-points after TNFα treatment (5, 10, 20, 40, 60, 120, 180, 240 min), medium has been removed and cells were washed with PBS immediately before mRNA and protein isolation.

2.1.1. mRNA preparation and real-time PCR
For isolation of total mRNA from hepatocytes the NucleoSpin RNA II kit has been used (Macherey-Nagel Düren, Germany). cDNA synthesis (RevertAid H minus, Fermentas, St. Leon-Rot, Germany) and semi-quantitative real-time PCR (Abgene/Thermo Fisher, Epsom, UK) have been performed using SYBR Green ROX Mix (Thermo Scientific, Ulm, Germany) according to the manufacturers’ protocol. The following primers were used in this study: IkBα forward: 5′-CCT GGC CAT CGT GGA GCA CT-3′, IkBα reverse: 5′-AGT AGG CCT GGT AGG TTA CC-3′; tubulin forward: 5′-TCA CTG TGC TGG AAG TTA CC-3′; tubulin reverse: 5′-GGG ACA TAG CCG TAA ACT GC-3′ (Thermo Scientific, Ulm, Germany). Cycling program: 95°C/15 min followed by 40 cycles 95°C/15 s and 60°C/1 min. Melting curve: 95°C/15 s, 60°C/30 s, 95°C/15 s.

2.1.2. Protein preparation, immunoprecipitation, and immunoblotting
Total protein fractions were collected at the indicated time-points using the Cell Lysis Buffer (Cell Signalling Technology, Frankfurt am M., Germany) supplemented with Protease Inhibitor Mix G (Serva, Heidelberg, Germany). After sonication (3 times for 20 s) and protein quantification (NanoDrop, Thermo Scientific), 80 µg/lane of total protein were loaded on a denaturing 10% PAA/SDS gel.

To determine time-dependent basal protein degradation of specific NFκB pathway constituents, cells were treated with cycloheximide (50 µg/ml). Proteins were isolated at indicated time-points.

For p65: IkBα-α co-immunoprecipitation, proteins were isolated using NP-40 buffer (50 mM Tris-HCl, 150 mM NaCl, 1% NP-40). Three micrograms of p65-specific antibody (clone F6, Santa Cruz Biotechnology, Heidelberg, Germany) and 40 µl G PLUS-Agarose (Santa Cruz Biotechnology) were mixed with 1.5 mg of total protein and incubated over-night. After centrifugation, the pellet was washed three times with HNTG buffer (20 mM Hepes pH 7.5, 150 mM NaCl, 0.1% Triton X-100, and 10% glycerol). Subsequently, the pellet was diluted in 1x sample buffer (100 mM Tris-HCl pH 6.8, 5% glycerol, 0.005% BBP, 5% SDS, 5% β-mercaptoethanol) and incubated at 95°C for 6 min. Pellet was pulled down and supernatant was loaded on a 10% PAA/SDS gel.

After protein transfer, membranes were blocked in 1x TBS containing 0.1% Tween and 5% BSA (Serva, Heidelberg, Germany) or 5% milk for 30 min. The respective primary antibodies were incubated over-night at 4°C. After washing with TBST, membranes were incubated with specific secondary antibody (1 h at RT) and signal detection was performed by ECL (Western Lightning Plus-ECL, Perkin Elmer). Signals were digitally documented using the Fluorochrome FC device (Alpha Innotech/Biozym, Hess. Oldendorf, Germany).

Primary antibodies used in this study were: anti-p65 (clone A, dilution for WB: 1:200, Santa Cruz Biotechnology), anti-p65 (clone F6; dilution for IP: 1:25, Santa Cruz Biotechnology), anti-phospho-p65 (Ser536, dilution for WB: 1:500, Santa Cruz Biotechnology), anti-IκBα-α (#9242, dilution: 1:750, Cell Signalling Technology), anti-phospho-IκBα (Ser32, clone: 14D4, dilution: 1:400, Cell Signalling Technology), and anti-actin (clone: C4, dilution: 1:2000, MP Biomedical, Germany). Secondary antibodies were: anti-rabbit IgG HRP-linked antibody (dilution: 1:2000, Cell Signalling Technology) and anti-mouse IgG (dilution: 1:2000, Cell Signalling Technology).

2.1.3. Data acquisition and processing
Every experiment was replicated at least eight times and raw data have been used for modeling purposes. For every protein, four digital pictures at different exposure times were taken and signals were quantified using the image analysis software Quantity-One (Bio-rad, Munich, Germany). Each numerical data point was normalized to respective actin amounts, which served as loading control for the samples. For comparability between different experiments, all data points were further normalized to the appropriate control on each blot (hepatocytes without TNFα stimulation) to a fixed value (c = 100 arbitrary units).

2.2. COMPUTATIONAL
A system of ordinary differential equations (ODEs) was set up with the software COPASI (Hoops et al., 2006) and integrated using the LSODA integrator as implemented in this software (Petzold, 1983). Sensitivity analysis was employed to determine the influence of certain parameters on systems outcomes, e.g., amplitudes as described in the text. The sensitivity analysis was also used as implemented in COPASI. Parameter fitting was performed using the particle swarm algorithm (Kennedy and Eberhart, 1995), again as implemented in COPASI.

3. RESULTS
3.1. INITIAL TNFα/NFκB SIGNALING MODEL
In order to investigate hepatocyte-specific behavior of NFκB signaling, we developed an initial model based on the most important NFκB pathway constituents reported in the literature for hepatocytes (Wullaert et al., 2007; Figure 1A). The involved processes were modeled similar to published models (O’Dea et al., 2007; Ashall et al., 2009). All processes upstream of the IkB kinase (IKKβ) were lumped in the model assuming that they happen very fast (Delhase et al., 1999). Phosphorylated IKKβ is active and phosphorylates free and p65-bound IκBα. Phosphorylated IκBα dissociates
from p65, and is rapidly degraded (Ghosh et al., 1998). Free p65 is imported to the nucleus where it induces transcription of different target genes such as IκBα and A20 (Scott et al., 1993; Tian et al., 2005). In our initial model we introduced stimulated and basal transcription, translation, nuclear mRNA export, and degradation of IκBα as well as IκBα-mRNA. Newly synthesized IκBα can be phosphorylated and degraded or it can reenter the nucleus where it forms a complex with p65 which is then exported to the cytoplasm (Arenzana-Seisdedos et al., 1995). Furthermore, p65 turnover was included in form of translation and degradation reactions while assuming a constant concentration of the corresponding mRNA. Most reactions were modeled as reversible reactions with mass action kinetics, while phosphorylation of complexed and free IκBα was modeled by a Michaelis-Menten kinetics with IKKβ being the catalytic enzyme in this term. The included protein synthesis and degradation for p65 and IκBα, and the reversible kinetics as well as a basal IKKβ phosphorylation led to basal levels of all species with exception of the ligand TNFα. We assumed the model to be in a steady-state before administration of TNFα. For more details on the reactions and the parameters see Tables S1, S3, S5–S7 in Supplementary Material.

3.2. PARAMETRIZATION OF THE MODEL BASED ON EXPERIMENTAL DATA

To parametrize the initial model of TNFα-induced NFκB signaling, quantitative time-courses of NFκB pathway constituents were measured after TNFα treatment of primary murine hepatocytes. Since it has been shown that TNFα operates very early during liver regeneration (Fausto et al., 2006), we investigated the system for 4 h after TNFα stimulation and measured concentrations and/or activities using narrow time-point sampling, especially in the beginning of this time frame.

We detected the phosphorylation of IκBα and p65 by immunoblotting using total cellular lysates isolated at different time-points after TNFα stimulation. Rather constant levels during the time-course were observed (data not shown). However, TNFα stimulation resulted in a rapid increase of phosphorylated p65 after 10 min, followed by a strong decrease until the original level was reached after approximately 40 min (Figure 1B). IκBα was phosphorylated approximately with the same dynamics as p65; however, slightly faster and with a second peak of activation around 60 min, which lasted until 120 min after stimulation (Figure 1B).
In line with the notion that phosphorylation of IκBα is associated with K48-linked polyubiquitination and subsequent degradation, a rapid reduction of the IκBα protein level from 10 to 40 min after TNFα treatment and fast recovery after 60 min until the end of the experiment were detected (Figure 1B). To determine to what extent the p65 activity triggered IκBα gene transcription, real-time PCR analysis was performed revealing increased IκBα mRNA levels starting from 20 min with a maximum peak level around 60 min after stimulation. These experimental data were used to perform parameter estimation for the initial model.

To further constrain the parameters of the model, basal turnover of the examined signaling components was measured. For this primary mouse hepatocytes were pretreated with the inhibitor of protein synthesis cycloheximide (CHX) and time-courses up to 360 min without TNFα administration were measured for p65 and IκBα by immunoblotting (Figure 2A). The results revealed high p65 stability throughout the entire experimental time frame, indicating little or no p65 turnover. On the other hand, IκBα showed a 40% degradation within 6 h after CHX treatment (Figure 2B). Therefore, a constraint was introduced for parameter estimation to only consider parameter sets that ensured a stable level of p65. Individual parameter values for the degradation of p65 and IκBα in their different binding states could not be derived from the measurements of total p65 and IκBα concentrations. Instead, parameters of p65 and IκBα degradation were constrained in the parameter fitting procedure such that the resulting overall degradation rates were close to the measured values.

The initial model was able to fit most of the data well. The fitting, which was computationally very time consuming, was repeated 60 times with random start values, the 30 best fits were selected for further analysis. However, a more detailed inspection of the resulting model trajectories revealed that simultaneous fitting of phosphorylated p65, IκBα mRNA, and IκBα time-courses was not sufficiently possible with this preliminary model. More specifically, considering the time-courses of phosphorylated p65, phosphorylated IκBα, and total IκBα revealed two distinct clusters of parameter sets, none of which could capture all the features of the observed data. In the first cluster of parameter sets only the initial fast increase of phosphorylated p65 was captured, the following equally fast decrease however was predicted to be slower than the experimental data would suggest; furthermore, IκBα levels in the model did not decrease as strong as the experimental data would suggest. In the second group of parameter sets the dynamics of phosphorylated p65 were captured better, while total IκBα levels went into a too strong overshoot above the steady-state concentration at approximately 100 min. Also the amplitude of the IκBα mRNA dynamics was significantly smaller than the measurements suggested. These inconsistencies are due to a tight coupling of free p65 and IκBα levels in the initial model and cannot be resolved without changes to the model structure.

3.3. EXTENDED MODEL INCLUDING ADDITIONAL p65 PHOSPHORYLATION

To resolve these discrepancies and improve the description of the experimentally observed induction of IκBα mRNA and subsequent protein levels, we introduced into the initial model reactions that could modify the transcriptional activity of p65 in the nucleus. Since besides phosphorylation at serine 536 additional phosphorylations of p65 were captured better, while total IκBα levels went into a too strong overshoot above the steady-state concentration at approximately 100 min. Also the amplitude of the IκBα mRNA dynamics was significantly smaller than the measurements suggested. These inconsistencies are due to a tight coupling of free p65 and IκBα levels in the initial model and cannot be resolved without changes to the model structure.

3.4. IMPACT OF PROTEIN TURNOVER ON THE DYNAMICS OF TNFα/NFκB SIGNALING

The role of protein turnover has been neglected in most of the studies involving NFκB signaling. However, IκBα degradation might be a critical step because its protein levels immediately decreased after activation of the system (IκBα phosphorylation). In addition, the system's main activated effector, p65, is in turn able to increase IκBα protein levels by promoting its transcription, thus establishing a negative feedback loop in the system.

Therefore, we computationally analyzed the impact of protein degradation and turnover on important signaling readouts such as the amplitude peak of phosphorylated p65 or the integrated
response (area under curve) which represent the signal strength. The ensemble of model parametrizations produced by 30 independent fits was analyzed again. Each of these parametrizations was subjected to a sensitivity analysis calculating the impact of specific kinetic parameters and protein turnover on the peak-height (amplitude) as well as integrated response of the signal (concentration of NFκB). The results demonstrated that the properties of these models were surprisingly robust as depicted in Figure 4 (for the respective heat maps of the IκBα, phosphorylated IκBα, and IκBα mRNA amplitude and integral see Figures A1–A3).

These heat maps showed a high consistency within the 30 different fits despite the unidentifiability of most parameters, indicating that these sensitivities were valid for most parameter sets and therefore most likely for physiological parameter sets. Interestingly, few parameter sets, e.g., parameter set 30, showed differences in comparison with most parameter sets. Analyzing the specific behavior of these unique models, revealed a high sensitivity toward many parameters, indicating these systems to be in an unstable state with respect to perturbation. Therefore, it can be assumed that these few models, although representing the data well, do not correspond to the physiological states in cells.

When analyzing especially the parameters involved in protein synthesis and degradation, which regulate protein level, it became apparent that among the prominent parameters influencing the integral of the signal were those involved in transferring the TNFα stimulation into phosphorylated p65 liberation in form of IκKβ phosphorylation (parameters 24, 26, 27 in Figure 4) and p65 translation and degradation (parameters 42, 37). Interestingly, changing translation and degradation of p65 proportionally, so that turnover was changed but the protein level stayed constant, showed very little impact (parameter 50). Parameters describing basal IκBα transcription, translation, and turnover (parameters 22, 23, 49) were also influencing the integral drastically, whilst its degradation and active transcription (parameters 7–10, 19–21) showed very little impact.

Among the parameters determining the signal amplitude were degradation and translation of p65 (parameters 37, 42); again, despite its turnover (parameter 49) having very little influence. In general, the amplitude of phosphorylated p65 was controlled by fewer parameters than the integral of phosphorylated p65.

With respect to the amplitudes and integrals of phosphorylated p65, total IκBα, phosphorylated IκBα, and IκBα mRNA, the system typically depended on the p65 translation and degradation (parameters 37, 42), the activated IκKβ phosphorylation (parameters 24, 26), and the IκBα mRNA degradation in the cytoplasm (parameter 11), whilst changing p65 turnover (assuming unchanged steady-state levels of p65, parameter 49) had limited impact.

3.5. VALIDATION OF THE MODEL AND PREDICTION OF COMPLEX FORMATION

To assess improvements achieved through the development of the extended model, we compared the ratios of free IκBα before TNFα administration predicted by the initial model and the extended model. In the initial model all parameters sets propose that at least 50% of total IκBα is in an unbound state. On the other hand in the extended model the median lies at 20% (Figure 5) which is well in line with the experimentally observed 15% reported by Rice (1993).

Finally, we validated our mathematical model of TNFα-induced NFκB signaling in primary mouse hepatocytes by using experimental data not utilized for parametrization of the model. p65:IκBα co-immunoprecipitation was performed to measure...
complexed p65 concentrations over time (Figure 6B). Since most of the parameter values were not identifiable, we created a model ensemble by conducting the parameter fitting 30 times. All 30 fits, representing different parameter sets all fitting the experimental data, were used to predict the observed parameter sets were clustered hierarchically according to the shown sensitivities, however, this is merely to improve visual survey and there is no direct correlation to the similarity of parameters. The clustering was preformed with the help of the software Cluster 3.0 (de Hoon et al., 2004).

The experimental results showed the initial level of p65:IkBα complexes strongly decreased 5 to 10 min after stimulation with experimental co-immunoprecipitation data. For this purpose, the kinetic parameters were kept unchanged; only the scaling factors were refitted to the validation data (Figure 6A).

The experimental results showed the initial level of p65:IkBα complexes strongly decreased 5 to 10 min after stimulation with
TNFα. During this time frame, concentrations of serine 536 phosphorylated p65 increased and IκBα concentration decreased, while after 40 min the IκBα and complex concentrations increased again. Between 60 and 120 min the complexed p65:IκBα reached their initial level, followed by a second minor decrease. The model predicted the full dynamics until the second decrease at approximately 180 min, which was likely due to additional feedback loops in the system.

4. DISCUSSION

The involvement of NFκB signaling is critical in the context of liver injury and regeneration as well as inflammation and tumorigenesis (Luedde and Schwabe, 2011). Especially during chronic liver disease, activation of this pathway triggers hepatocyte proliferation and (at later time-points) is eventually supporting tumor development and progression. Hepatocellular carcinoma (HCC) is the third most common cause of cancer-related death worldwide (Breuhahn et al., 2011) and represents a paradigm of inflammation-induced cancer, indicating a strong link between activation of pro-inflammatory pathways such as TNF-induced NFκB signaling and tumorigenesis. However, the impact of NFκB signaling on early phases of hepatocarcinogenesis is highly complex, since this pathway is activated in different cell types including hepatocytes (which represent the major cell population), hepatic stellate cells, and resident immune cells (Kupffer cells) (Amann et al., 2009). In order to understand the impact of this pathway in the earliest stages of liver damage and tumorigenesis, it is of central relevance to generate mathematical models describing its dynamic behavior in normal and non-malignantly transformed cells. These tools represent the basis for further comprehensive systems biology studies, essential for a deeper understanding of liver cancer initiation and progression.

Our initial model for TNFα-induced NFκB signaling in mouse hepatocytes was constructed by applying central aspects of established computational models of NFκB signaling in other organisms or cell types (O’Dea et al., 2007; Ashall et al., 2009). Our goal was a reparametrization of this model using hepatocyte-specific experimental data obtained from comprehensive, quantitative, and time-resolved protein and transcript analyses. However, the model was not able to satisfactorily fit all experimental data simultaneously. Specifically, it was not able to describe the difference in the dynamics of phospho-p65 and free IκBα concentrations during the first hour after administration of TNFα. While the initial rise of phospho-p65 and the corresponding decrease of IκBα occur on a similar fast time scale, phospho-p65 returns to near its steady-state value faster than IκBα. In the initial model, the dephosphorylation of p65 is assumed to coincide with its binding to IκBα implying it cannot happen faster than the regeneration of IκBα. Since this is contrary to our observations, we uncoupled p65 dephosphorylation from its binding to IκBα by introducing a more detailed description of p65 phosphorylation and dephosphorylation including a state in which p65 is not phosphorylated but also not bound to IκBα in the nucleus.

It is well known that p65 can be phosphorylated by a number of different kinases at different residues such as serine 536, which is measured by our immunoblotting approach (Viatour et al., 2005). Among the different kinases that may effect serine 536 phosphorylation, only IKKβ is activated by TNFα-induced signaling (Viatour et al., 2005). This is the process that is implicitly included in our initial model. The extended model contains in addition the
phosphorylation of p65 at serine 276 by a nuclear kinase. Our data suggests uncoupling of p65 phosphorylation and its binding to IκBα, which was achieved by implementing an additional phosphorylation and corresponding dephosphorylation process in the model. Adjusted like this, the model can indeed reproduce the observed differences in the dynamics of phospho-p65 and free IκBα. In addition, the revised model also convincingly reproduced the amplitude of the IκBα mRNA measurements, which was not possible using the initial model.

A potential candidate for such a nuclear kinase could be mitogen- and stress-activated protein kinase 1 (MSK1) that has also been shown to be expressed in human liver cells (Deak et al., 1998). However, MSK1 appears to have no direct impact on IκBα expression and the phosphorylation of p65 by MSK1 is controversially discussed (Joo and Jetten, 2008).

The extended model is able to explain features of NFκB signaling in hepatocytes as displayed by our measurements. However, NFκB signaling is known to involve more constituents and regulations than considered in this study. Therefore, other components can be included in future research. Tumor necrosis factor α-induced protein 3 (TNFAIP3/A20) is one considerable protein, involved in a negative loop inhibiting p65 phosphorylation acting upstream of IKK-β (Opipari et al., 1990). This protein, together with IκBα is probably the most important factor in the acquisition of phosphorylated p65 oscillatory behavior critical for transcriptional target fate (Ashall et al., 2009). Another NFκB constituent involved in negative feedback loop with high impact in NFκB signaling oscillations is IkBε. This protein belongs to the IκB inhibitor family of signaling whose activity has been detected later and out of phase if compared with IκBα. This special feature leads IκBε to dampen the effect of IκBα during the last phase of sustained NFκB activity and to mediate the terminations of the signaling in response to transient stimulation (Kearns et al., 2006). From our preliminary data, both protein TNFAIP3/A20 and IκBε present a significant expression in primary hepatocytes following TNFα stimulation and this data will be used for parameterization of further improved models. Moreover signals coming not directly from TNFα but able to fine-tune the system especially in the nucleus should be taken into account.

A vital methodological question remains in the context of this work: What is the justification to claim that the model proposed here is a model for NFκB signaling in mouse hepatocytes? We have consulted literature to make sure all the processes and components included in the model are actually present in mammalian hepatocytes. On the other hand, to our knowledge none of these components or processes is actually exclusive to liver cells or hepatocytes. Basically this leaves the parametrization of the model as being hepatocyte-specific. Parameter estimation was performed with data measured in murine hepatocytes and the presented model was able to fit the data satisfyingly. However, some of the parameters are unidentifiable with the available data, i.e., for different values of the parameter the model fits the data equally well. Instead of eliminating the unidentifiabilities – by performing additional experiments and/or by simplifying the model – here we focused on making predictions from the model that are valid for all parametrizations of the model that are compatible with the experimental data. As a pragmatic way to characterize the set of parameter values that let the model fit the data, a heuristic sampling of parameter space was performed, a technique that was recently applied in other studies (Maiwald et al., 2010; Levering et al., 2012; Wegner et al., 2012). The parameter estimation process was repeated 30 times, each time starting with different random parameter values as initial guess, resulting in 30 different sets of parameters that are compatible with the experimental data. This immediately results in a good estimate for the identifiability of the different parameters: the more the parameters differ between the repeated parameter estimation runs the less identifiable they are.

For drawing conclusions from our model or creating predictions for validation we need to make sure that these conclusions or predictions are valid for all or at least most of the 30 parameter sets. Indeed, the model validation described in the Results section proved to be conserved for all 30 parameter sets. Similarly the sensitivities that were calculated in order to study the role of protein turnover turned out to be consistent for 25 of the 30 parameter sets. While of course we cannot be absolutely certain from using only a limited number of samples, we can confidently claim that typically the model will predict a certain behavior of NFκB signaling in hepatocytes whenever the parameters are chosen so that it fits the data.

While our model shares its basic structure with most relevant NFκB models in literature, it is based on NFκB dynamics following TNFα stimulation in murine primary hepatocytes. Our experimental setup allows us to disturb hepatocytes with different combination of ligands and to compare data with prediction from our model. Different models for different signaling pathways essential for liver homeostasis and response to injury are currently being developed, e.g., within the German Virtual Liver Network (VHN). In this context our model can be a useful tool for comparison and integration of different models. Thus, we have established a mathematical model for TNFα/NFκB signaling in primary mouse hepatocytes that indicated the importance of basal turnover of the pathway components for the dynamic behavior and facilitated the prediction of the kinetics of complex formation in the pathway. Taken together the model provides an important building block to unravel regulation of liver regeneration and the impact of inflammatory responses across the scales.

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SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at http://www.frontiersin.org/Systems_Biology/10.3389/fphys.2012.00466/abstract

Table S1 | Ordinary differential equations describing all species in the original model. As initial concentrations the steady-state concentrations were used.

Table S2 | Ordinary differential equations describing all species in the model expanded by p65 phosphorylation.
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APPENDIX

1. \(k_1\): complex association
2. \(k_2\): complex association
3. \(k_1\): complex nuclear shuttle
4. \(k_2\): complex nuclear shuttle
5. \(k_{cat}\): IkB\(\alpha\) complex phosphorylation
6. \(k_M\): IkB\(\alpha\) complex phosphorylation
7. \(k\): IkB\(\alpha\) degradation complex cytoplasm
8. \(k\): IkB\(\alpha\) degradation complex nucleus
9. \(k\): IkB\(\alpha\) degradation cytoplasm
10. \(k\): IkB\(\alpha\) degradation nucleus
11. \(k\): IkB\(\alpha\) − mRNA degradation cytoplasm
12. \(k\): IkB\(\alpha\) − mRNA degradation nucleus
13. \(k\): IkB\(\alpha\) degradation
14. \(k\): IkB\(\alpha\) − mRNA degradation
15. \(k\): IkB\(\alpha\) − mRNA transport
16. \(k\): IkB\(\alpha\) nuclear shuttle
17. \(k\): IkB\(\alpha\) nuclear shuttle
18. \(k\): IkB\(\alpha\) nuclear shuttle
19. \(k\): IkB\(\alpha\) nuclear shuttle
20. \(k\): pIkB\(\alpha\) active degradation
21. \(k\): pIkB\(\alpha\) active degradation
22. \(k\): pIkB\(\alpha\) active degradation
23. \(k\): pIkB\(\alpha\) active degradation
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47. \(k\): pIkB\(\alpha\) active degradation
48. \(k\): pIkB\(\alpha\) active degradation
49. \(k\): pIkB\(\alpha\) active degradation
50. \(k\): pIkB\(\alpha\) active degradation

Parameter sets

FIGURE A1 | Impact of parameter changes on amplitude and integral of IkB\(\alpha\). For each of 30 parameter sets the sensitivities with respect to every model parameter are shown in a heat map. Blue shades denote negative, red shades positive sensitivity coefficients. Color shading is scaled from -1.0 to +1.0. The parameter sets were clustered hierarchically according to the shown sensitivities, however, this is merely to improve visual survey and there is no direct correlation to the similarity of parameters. The clustering was preformed with the help of the software Cluster 3.0 (Ashall et al., 2009).
FIGURE A2 | Impact of parameter changes on amplitude and integral of phospho-IκBα. For each of 30 parameter sets the sensitivities with respect to every model parameter are shown in a heat map. Blue shades denote negative, red shades positive sensitivity coefficients. Color shading is scaled from −1.0 to +1.0. The parameter sets were clustered hierarchically according to the shown sensitivities, however, this is merely to improve visual survey and there is no direct correlation to the similarity of parameters. The clustering was performed with the help of the software Cluster 3.0 (Ashall et al., 2009).
1. $k_1$: complex association
2. $k_2$: complex association
3. $k_1$: complex nuclear shuttle
4. $k_2$: complex nuclear shuttle
5. $k_{cat}$: IkBα complex phosphorylation
6. $k_1$: IkBα complex phosphorylation
7. $k_2$: IkBα degradation complex cytoplasm
8. $k$: IkBα degradation complex nucleus
9. $k$: IkBα degradation cytoplasm
10. $k$: IkBα degradation nucleus
11. $k$: IkBα mRNA degradation cytoplasm
12. $k$: IkBα mRNA degradation nucleus
13. $k$: IkBα mRNA transport
14. $k$: IkBα degradation
15. $k$: IkBα degradation
16. $k$: IkBα degradation
17. $k$: IkBα degradation
18. $k$: IkBα degradation
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48. $k$: IkBα degradation
49. $k$: IkBα degradation
50. $k$: IkBα degradation

FIGURE A3 | Impact of parameter changes on amplitude and integral of IkBα mRNA. For each of 30 parameter sets the sensitivities with respect to every model parameter are shown in a heat map. Blue shades denote negative, red shades positive sensitivity coefficients. Color shading is scaled from −1.0 to +1.0. The parameter sets were clustered hierarchically according to the shown sensitivities, however, this is merely to improve visual survey and there is no direct correlation to the similarity of parameters. The clustering was performed with the help of the software Cluster 3.0 (Ashall et al., 2009).