THEORETICAL EMISSION SPECTRA OF ATMOSPHERES OF HOT ROCKY SUPER-EARTHS

YUICHI ITO1, MASAHIRO IKOMA1, HAJIME KAWAHARA1, HIROKO NAGAHARA1, YUI KAWASHIMA1, AND TAISHI NAKAMOTO2

1 Department of Earth and Planetary Science, The University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113-0033, Japan
2 Department of Earth and Planetary Sciences, Tokyo Institute of Technology, 2-12-1 Ookayama, Meguro-ku, Tokyo 152-8551, Japan

Received 2014 July 4; accepted 2015 January 19; published 2015 March 12

ABSTRACT

Motivated by recent detection of transiting high-density super-Earths, we explore the detectability of hot rocky super-Earths orbiting very close to their host stars. In an environment hot enough for their rocky surfaces to be molten, they would have an atmosphere composed of gas species from the magma oceans. In this study, we investigate the radiative properties of the atmosphere that is in gas/melt equilibrium with the underlying magma ocean. Our equilibrium calculations yield Na, K, Fe, Si, SiO, O, and O2 as the major atmospheric species. We compile the radiative absorption line data of those species available in the literature and calculate their absorption opacities in the wavelength region of 0.1–100 μm. Using them, we integrate the thermal structure of the atmosphere. Then, we find that thermal inversion occurs in the atmosphere because of the UV absorption by SiO. In addition, we calculate the ratio of the planetary to stellar emission fluxes during secondary eclipse, and we find prominent emission features induced by SiO at 4 μm detectable by Spitzer, and those at 10 and 100 μm detectable by near-future space telescopes.

Key words: planets and satellites: atmospheres – planets and satellites: composition – planets and satellites: terrestrial planets

1. INTRODUCTION

We have recently entered a new era of characterizing the atmospheres of low-mass exoplanets with masses of \( \lesssim 30 M_J \). Transmission and/or emission spectra have been obtained for several low-mass exoplanets in transit (e.g., Deming et al. 2007; Bean et al. 2010). Most of them are less dense than would be if they were composed of silicate. Characterization of the relatively thick atmospheres of such exoplanets has been paid attention to as a first stepping-stone toward an observational science of habitable planets.

A next stepping-stone would be detection and characterization of thin atmospheres of close-in low-mass exoplanets, the observed mass-radius relationships for which are consistent with theoretical ones for rocky planets (e.g., Fortney et al. 2007; Valencia et al. 2007; Grasset et al. 2009). In particular, of special interest in this study are rocky super-Earths with masses of \( \lesssim 10 M_J \) and radii of \( \lesssim 2 R_J \) that are orbiting so close to their host stars that their surface temperatures are above the vaporization temperature of rock, because of intense stellar irradiation. Such exoplanets are referred to as hot rocky super-Earths (HRSEs, hereafter) in this study. Examples of the transiting HRSEs detected so far are CoRoT-7b (Léger et al. 2009), Kepler-10b (Batalha et al. 2011), Kepler-78b (Howard et al. 2013), and 55 Cnc e (Winn et al. 2011). They are likely to have atmospheres with chemical species of rocky origin.

Based on their chemical equilibrium calculations, Schaefer & Fegley (2009) presented the possible compositions of the “silicate atmosphere” that is in gas-melt equilibrium with the molten rocky surface with no highly volatile elements such as H, C, N, S, and Cl (i.e., volatile-free magma ocean). They considered temperatures, \( T \), of 1500–3000 K and gravity of 36.2 m s\(^{-2}\), which corresponded to the planetary properties for CoRoT-7b, and assumed several compositions for the volatile-free magma, including the Earth’s continental and oceanic crusts, the bulk silicate Earth (BSE), and the bulk silicate moon. Their calculations demonstrated that the atmosphere contained Na, O, O2, and SiO as the major constituents. Also, they investigated changes in atmospheric composition due to partial loss of the atmosphere and found that Na was selectively lost from the atmosphere, while Mg became more abundant with fractional loss.

Miguel et al. (2011) made a similar but more extensive investigation of the composition of atmospheres of volatile-free HRSEs. They considered wider ranges of temperature (1000–3500 K), planetary mass (1–10 \( M_J \)), and planetary radius (1–2.5 \( R_J \)). Also, they considered komatiite in addition to BSE for the magma material. The resultant atmospheric compositions are basically similar to those from Schaefer & Fegley (2009): the major constituents are Na, O, O2, and SiO, although Fe and Mg are more abundant than SiO at \( T \lesssim 2000 \) K. They defined five types of HRSE atmosphere, depending on the abundance of the six species, and then classified Kepler planet candidates with radii of \( \lesssim 2.5 R_J \), according to type.

Since the presence of such atmospheres is specific to rocky planets, observational detection of those atmospheres could add a piece of convincing evidence for rocky planets. Furthermore, identifying the atmospheric constituents could give constraints on the bulk composition and formation process of HRSEs. However, the properties and detectability of the atmospheres of the volatile-free HRSEs have not been examined yet (see Schaefer et al. (2012) and Lupu et al. (2014) for the volatile-rich cases). Thus, the aim of this study is to identify the radiative properties of the atmospheres on top of the global magma oceans of volatile-free HRSEs and then assess their detectability. (In this study, we call such an atmosphere a mineral atmosphere.)

To this end, we model the thermal structure of the mineral atmospheres of HRSEs. The composition of the atmosphere is obtained numerically in Section 2. Also, we compile the absorption-line data for the major gas species, which are published in the literature or online, and then calculate the absorption opacities in Section 3. Using the chemical
compositions and absorption opacities, we integrate the thermal structure of the irradiated atmosphere in radiative equilibrium in Section 4. Then, we evaluate the detectability of the chemical species in the mineral atmosphere through the emission spectra obtained during secondary eclipse in Section 5. Finally, we discuss several effects to be examined in Section 6 and then conclude this study in Section 7.

2. CHEMICAL COMPOSITION

2.1. Element Abundance and Gas Pressure

To calculate the element abundance and pressure of gas in gas/melt chemical equilibrium with silicate melt for a given temperature, we use the chemical equilibrium code MELTS (Ghiorso & Sack 1995; Asimov & Ghiorso 1998), which performs the free-energy minimization calculations. Figures 1 and 2 show the calculated total pressures and molar fractions of gas species, respectively, over a temperature range between 1500 and 3000 K for four magma compositions: (1) BSE, (2) the Earth’s mid-ocean ridge basalts (MORBs), (3) the Earth’s bulk crust, and (4) the Earth’s upper crust. The detail of the magma compositions is shown in Table 1. In this study, we consider the above four compositions of magma, following Schaefer & Fegley (2009), although the magma composition of exoplanets is uncertain. The actual magma composition depends not only on the element abundances but also on the thermal history of the planet; exploring the details is beyond the scope of this study. Note that the choice among the four magma compositions has little impact on the emission spectra in the infrared wavelength region. Detectable difference may arise in the visible emission spectra, which is discussed in Section 6.6.

The overall trend shown in Figures 1 and 2 is similar to that found by Schaefer & Fegley (2009) and Miguel et al. (2011), who used the MAGMA chemical equilibrium code (Fegley & Cameron 1987), instead of MELTS. For example, Na is the most abundant species in most of the temperature range, while SiO increases with temperature and becomes the most abundant one for $T \gtrsim 2800$ K for BSE and MORB. $T \gtrsim 2600$ K for the bulk crust, and $T \gtrsim 2500$ K for the upper crust. Also, the total vapor pressure is as small as $\sim 10^{-7}$ bars at $T = 1500$ K and $\sim 0.1$ bars at $T = 3000$ K, for example (see Figure 1).

A noticeable difference is seen in the abundance of potassium gas between our calculations and those by Schaefer & Fegley (2009) and Miguel et al. (2011). Our calculations yield much higher partial pressure of potassium: the ratio of the potassium to sodium partial pressures that we have obtained is larger by a factor of more than 100, relative to that calculated by Schaefer & Fegley (2009). This difference is due mainly to that in the adopted thermodynamic model for silicate melt. The melt model of MAGMA used in Schaefer & Fegley (2009) is ideal mixing of many simple and complex fictitious oxide species, which is calibrated for silicate melts with high-K$_2$O contents, whereas MELTS used in this study adopts a symmetric regular solution model with minimum melt components, which is calibrated by experimental results on natural systems with low-K$_2$O abundances. MAGMA would appropriately estimate potassium vapor pressure for high-K$_2$O melt, as shown in Figure 5 of Schaefer & Fegley (2004), but is not good for low-K$_2$O melt. By contrast, MELTS gives appropriate results for low-K$_2$O melt, which is of interest in this study (see Table 1). The impact on the emission spectrum from the mineral atmosphere is discussed in Section 6.6.

2.2. Gas-phase Equilibrium

To calculate the equilibrium abundances of gas species in the mineral atmosphere, we use the NASA CEA code (Gordon & McBride 1996), which performs the free-energy minimization calculations. In practice, we calculate the abundances for some selected temperatures from 2000 to 4500 K and pressures from $10^{-8}$ to $10^{-1}$ bars, which are of interest in this study, considering the gas-phase equilibrium of a system composed of only the major elements such as O, Na, K, Si, and Fe. We assume that the element abundances are vertically constant; their values are calculated in Section 2.1.

In our atmosphere model, the molar fractions of Na, K, and Fe gas vary little, compared to those of O, O$_2$, Si, and SiO. O$_2$ and SiO tend to decrease and O and Si increase with altitude in low-pressure regions in the atmosphere (see Section 4), because of thermal dissociations of O$_2$ and SiO.

Although we ignore photochemical reactions in this study, the photodissociation of SiO may be important for the detectability of the atmosphere. We discuss the possibility of the photodissociation of SiO and the impact on the atmospheric structure and detectability in Section 6.3.

3. ABSORPTION OPACITY

Among the chemical species shown in Figure 2, we consider line absorption by seven major species that include Na, K, Fe, O, O$_2$, Si, and SiO. We neglect Rayleigh scattering, because the Rayleigh scattering opacities are mostly smaller than the absorption opacity of SiO at wavelengths of interest in this study, as discussed in Section 6.1. Note that while TiO is known to be a strong absorber for visible rays (Plez 1998; Allard et al. 2000), its absorption opacity is always smaller than Na absorption opacity in the visible and IR wavelength regions, because the molar fraction of TiO is negligibly small (e.g., $\sim 10^{-12}$ at $T = 1500$ K and $\sim 10^{-6}$ at $T = 3000$ K), compared to that of Na ($\gtrsim 0.1$) in the atmosphere considered here.
Absorption opacities are calculated in the following way, except for O₂, for which we apply vibrational-rotational transitions in the HITRAN database (Rothman et al. 2013).

In local thermodynamic equilibrium, the absorption cross section of species A for an energy transition from the $i$th level to the $j$th level, $\sigma_{ij}^A$, is given as (Piskunov & Kupka 2001)

$$
\sigma_{ij}^A = g_i f_{ij} \frac{\pi e^2}{m_e c} \frac{1}{Q(T)} \left[ 1 - \exp \left( \frac{E_j - E_i}{kT} \right) \right] H(\nu, a),
$$

where $\nu$ is the frequency, $g_i$ is the statistical weight of the $i$th energy level, $f_{ij}$ is the oscillator strength for a transition from the $i$th (lower) to $j$th (higher) level, $E_i$ and $E_j$ are excitation energies of the $i$th and $j$th energy levels, respectively, and $Q(T)$ is the partition function of the species at temperature $T$. Parmeter $e$ is the elementary charge ($= 4.803 \times 10^{-10}$ esu), $m_e$ is the electron mass ($= 9.1094 \times 10^{-28}$ g), $c$ is the light-velocity ($= 2.9979246 \times 10^{10}$ cm s⁻¹), and $k$ is the Boltzmann constant ($= 1.3806488 \times 10^{-16}$ erg K⁻¹). We take the values of $g_i$, $f_{ij}$, and $E_i$ from Kurucz (1992) (see also Barton et al. 2013 for SiO). Also, we take the values of $Q(T)$ for Na, K, Fe, Si, and O from Irwin (1981) and for SiO from Rossi et al. (1985).

---

**Table 1**

| Oxide (wt%) | BSE a | MORB b | Bulk Crust b | Upper Crust b |
|-------------|-------|--------|-------------|--------------|
| SiO₂        | 45.1  | 49.6   | 60.6        | 66.6         |
| MgO         | 37.9  | 9.75   | 4.70        | 2.50         |
| FeO         | 8.06  | 8.06   | 6.71        | 5.04         |
| Al₂O₃       | 4.46  | 16.8   | 15.9        | 15.4         |
| CaO         | 3.55  | 12.5   | 6.41        | 3.59         |
| Na₂O        | 0.36  | 2.18   | 3.07        | 3.27         |
| Cr₂O₃       | 0.38  | 0.07   | 0.0004      | 0.0003       |
| TiO₂        | 0.20  | 0.9    | 0.72        | 0.64         |
| K₂O         | 0.03  | 0.07   | 1.81        | 2.80         |
| P₂O₅        | 0.02  | 0.10   | 0.13        | 0.15         |

a McDonough (1995).
b Rudnick & Gao (2003).

Figure 2. Composition of gas in chemical equilibrium with molten silicate. Molar fractions of the gas species are shown as functions of temperature. The assumed bulk compositions are the same as those of (a) the BSE, (b) the Earth’s MORB, (c) the Earth’s bulk crust, and (d) the Earth’s upper crust (see Table 1 for the details).
The function \( H(\nu, a) \) is the line profile function given by (e.g., Rybicki & Lightman 1986)
\[
H(\nu, a) = \frac{V(\nu, a)}{\sqrt{\pi} \Delta \nu_D},
\]
where \( a \) is the line width parameter, \( V(\nu, a) \) is the Voigt function, and \( \Delta \nu_D \) is the Doppler width given by
\[
\Delta \nu_D = \frac{v_0}{c} \sqrt{\frac{2kT}{m_A}},
\]
where \( m_A \) is the mass of the absorber and \( v_0 \) is the central frequency of the spectral line. The line width parameter \( a \) is calculated with damping constants for natural broadening and van der Waals broadening as (Piskunov & Kupka 2001)
\[
a = \frac{\Gamma_r + \Gamma_W}{4\pi \Delta \nu_D}
\]
According to Unsold (1955) and Gray (1976), \( \Gamma_r \) and \( \Gamma_W \) are given by
\[
\Gamma_r = 0.222 \times 10^{14} \lambda^{-2},
\]
\[
\Gamma_W = 17 \times \left[ 0.3 \times 10^{-30} \left( \frac{(l + 1)^2}{(l - \chi_j)^2} - \frac{(l + 1)^2}{(l - l)^2} \right) \right]^{2/5}
\times \nu^{3/5} N,
\]
where \( \lambda \) is wavelength in nm, \( N \) is the total number density of the gas species in \( \text{cm}^{-3} \), \( I \) is the ionization potential in eV, \( \chi_j \) is the excitation potential of the \( j \)th level in eV, and \( l \) is the electric charge. Parameter \( \nu \) is the relative thermal velocity defined by
\[
\nu = v_A \sqrt{1 + \frac{\mu}{\mu^A}},
\]
where \( v_A \) is the thermal velocity of the absorber and \( \mu^A \) and \( \mu \) are the molecular weight of the absorber and the mean molecular weight, respectively. As for the SiO absorption opacity, we assume \( \Gamma_W = 10^{-7} \times N \), following Kurucz & Avrett (1981). To calculate the line profile \( H(\nu, a) \) numerically, we use a polynomial expansion of the Voigt function given by Kuntz (1997). We have confirmed that this approximation yields relative errors of the order of \( 10^{-4} \), which is small enough for our discussion in this study.

Figure 3 shows the cross section of each species multiplied by each molar fraction as a function of wavelength for \( T = 2000 \) K (panel (a)) and \( 3000 \) K (panel (b)). The assumed pressures are \( 1.0 \times 10^{-5} \) bars for \( T = 2000 \) K and \( 0.01 \) bars for \( T = 3000 \) K. The magenta absorption is assumed to be BSE.

The calculated molar fractions of Na, K, Fe, Si, SiO, O, and O2 are, respectively, \( x_{Na} = 0.721 \), \( x_K = 0.0407 \), \( x_{Fe} = 0.001 \), \( x_{Si} = 10^{-6} \), \( x_{SiO} = 0.00731 \), \( x_O = 0.0233 \), and \( x_{O_2} = 0.189 \) for \( T = 2000 \) K (panel (a)) and \( x_{Na} = 0.204 \), \( x_K = 0.0142 \), \( x_{Fe} = 0.01 \), \( x_{Si} = 1 \times 10^{-3} \), \( x_{SiO} = 0.343 \), \( x_O = 0.0991 \), and \( x_{O_2} = 0.211 \) for \( T = 3000 \) K (panel (b)).

In Figure 3(a), the most abundant species Na (blue) presents a few hundred strong absorption lines between 0.253 and 10.0 \( \mu \)m, including the D line at 0.5893 \( \mu \)m. Also, several hundred strong lines of K (magenta) that are distinguishable from the Na lines are also found between 0.286 and 10.0 \( \mu \)m, including potassium doublet lines at 0.766 and 0.770 \( \mu \)m. While SiO (red) is less abundant by a factor of about 100 than Na, millions of its electron-transition absorption lines dominate in the far-UV (FUV) wavelength region (0.14–0.3 \( \mu \)m), and its absorption due to rotation-vibration transition dominates in several parts of the IR wavelength region, except narrow line peaks of Na, K, and Fe. The O electron-transition absorption (cyan) dominates between 0.10 and 0.13 \( \mu \)m. The several thousands of lines of Fe (gray) dominate between 0.20 and 0.54 \( \mu \)m. Although O2 (green) is the second most abundant species, its absorption is obscured by the other absorptions except at a narrow range around 30 \( \mu \)m. Also, the Si electron-transition absorption (yellow) is obscured by the SiO absorption in both Figures 3(a) and (b) and presents many prominent absorption lines between 0.1 and 0.3 \( \mu \)m.

In the higher-\( T \) case shown in Figure 3(b), the SiO feature is more prominent. The electron-transition absorption in the FUV region is larger by about two orders of magnitude than that in Figure 3(a), because the molar fraction of SiO is larger by two orders of magnitude (see Figure 2) and comparable with Na at 3000 K. The most remarkable difference in absorption feature between Figures 3(a) and (b) is that the SiO rotation-vibration absorption dominates at all the wavelengths longer than about 3 \( \mu \)m, except for several hundreds of narrow lines of Na and K. The rises in the peak values of SiO are due to the increase in abundance, while the enhancement of pressure broadening also contributes to the rises in absorption between those peaks.

Other minor species might contribute to the opacity. As for Mg and P present in Figure 2, we have confirmed that the absorption opacities of these species are negligibly small relative to the SiO absorption opacity in most of the wavelength region of interest, except for narrow ranges between 0.1 and 0.15 \( \mu \)m. Absorption-line data of the diatomic molecules other than SiO in Figure 2 are unavailable, to our knowledge. Thus, we have ignored their contribution.

Finally, for integrating the thermal structure of the atmosphere in the next section, we use the total absorption opacity, \( \kappa_{\nu} \), calculated as
\[
\rho \kappa_{\nu} = N \sum_A x_A \sigma_{ij}^A (i, j),
\]
where \( \rho \) is the mass density.

4. TEMPERATURE PROFILE

In this study, we simulate the one-dimensional plane-parallel thermal structure of the atmosphere that is in the radiative, hydrostatic, and chemical equilibrium. To do so, we integrate the so-called two-stream equations with the assumption of quasi-isotropic radiation, adopting the \( \delta \)-Eddington approximation (Toon et al. 1989):
\[
\frac{dF_{\nu}^+}{d\tau_{\nu}} = 7 \frac{F_{\nu}^+}{4} - \frac{1}{4} F_{\nu} - 2 \pi B_{\nu}(T),
\]
\[
\frac{dF_{\nu}^-}{d\tau_{\nu}} = -\frac{1}{4} F_{\nu}^+ - 7 \frac{F_{\nu}^-}{4} + 2 \pi B_{\nu}(T),
\]
where \( F_{\nu}^+ \) and \( F_{\nu}^- \) are the upward and downward radiative fluxes, respectively, \( B_{\nu}(T) \) is the Planck function, and \( \tau_{\nu} \) is the
Optical depth defined by

\[ \frac{d\tau_\nu}{dz} = -\kappa_\nu \rho, \]  

where \( z \) is the altitude. In Equations (9) and (10), we have assumed that the single-scattering albedo is 0, because absorption dominates scattering in most of the wavelength region of interest, as described above. The boundary conditions at the top and bottom of the atmosphere are, respectively, \( F_\nu^r = 0 \) and \( F_\nu^{r+} = \pi B_\nu (T_g) \), where \( T_g \) is the ground temperature. To solve Equations (9) and (10), we have used the widely used algorithm developed by Toon et al. (1989). According to Toon et al. (1989), the error in the radiative fluxes caused by the two-stream approximation was typically less than 10%, which is small relative to uncertainties in physical properties of exoplanets.

The net radiative flux integrated over all frequencies is constant throughout the atmosphere in radiative equilibrium. For an irradiated atmosphere, the net radiative flux, \( F_{\text{net,}\nu} \), is written as

\[ F_{\text{net,}\nu} (\tau_\nu) = F_\nu^{+} (\tau_\nu) - F_\nu^{-} (\tau_\nu) - \mu_\nu F_\nu^{-} e^{-\tau_{\nu,0}}, \]  

where \( F_\nu^{+} \) is the incident stellar flux and \( \mu_\nu \) is the cosine of the zenith angle of the incident stellar radiation. The radiative equilibrium condition is given as

\[ \int_0^\infty F_{\text{net,}\nu} d\nu = F_0, \]  

where \( F_0 \) is the constant flux. An HRSE is subject to tidal heating. Its strength depends on orbital and internal properties of the HRSE (Barnes et al. 2010). The detailed consideration of the tidal heating effect is beyond the scope of this study (a brief discussion is made in Section 6.4). In this study, we assume \( F_0 = 10 \text{ W m}^{-2} \) for numerical stability. For \( F_0 < 10 \text{ W m}^{-2} \), we have confirmed that choice of \( F_0 \) has little influence on the thermal structure of the atmosphere.

We consider a pressure range from \( 1 \times 10^{-8} \) bars to the pressure at ground level, \( P_g \). Note that \( P_g \) is determined a posteriori, because \( P_g \) is the vapor pressure, which depends on the ground temperature, \( T_g \). Numerically, the atmosphere is vertically divided into 50 layers. The layers are prepared so that the size of each layer logarithmically increases with pressure. In addition, to integrate Equations (9) and (10), we consider 100 spectral intervals in a frequency range between \( 1 \times 10^{13} \) and \( 2 \times 10^{15} \text{ s}^{-1} \) such that the size of each interval logarithmically increases with frequency. We calculate the harmonic mean opacities using cross sections obtained in Section 3. The calculation method of the mean opacities is described in the Appendix.

To find the thermal structure of the atmosphere in radiative equilibrium and also in gas-melt chemical equilibrium with the underlying magma ocean, we need three iterative procedures. First, to find the radiative equilibrium solution for given opacities and molar fractions of atmospheric gases, we integrate the equation of energy conservation,

\[ \frac{dT_n}{d\bar{\nu}} = \frac{dF_n}{dP_n}, \]  

where \( \bar{\nu} \) is a normalized time and \( T_n, P_n, \) and \( F_n \) are the temperature, pressure, and net radiative flux in the \( n \)th layer, respectively. The integration is continued until \( |F_n - F_0|/F_0 \) becomes smaller than 1% in all the layers.

Second, once we find the radiative equilibrium solution, we calculate the opacities that are consistent with temperatures obtained above. In practice, to save memory and CPU time, we have prepared a numerical table in which the harmonic mean opacities (see the Appendix) in 100 spectral intervals are given as functions of \( T, \log P, \) and the mean molecular weight, \( \bar{\mu} \); the grids are prepared for \( T = 2000, 2500, 3000, 3500, 4000, \) and \( 4500 \text{ K}, \log (P/\text{bar}) = -1, -2, -3, -4, \) and \(-5, \) and \( \bar{\mu} = 25, 30, \) and 35. In the pressure range from \( 1 \times 10^{-8} \) to \( 1 \times 10^{-5} \) bars, we have ignored the pressure dependence of the opacity because \( \Gamma_\nu > \Gamma_W \) in the range. Note that we have checked that the calculated flux differs by at most 5%, even if a smaller table with \( T = 2000, 3000, \) and \( 4000 \text{ K}, \log (P/\text{bar}) = -1, -3, \) and \(-5, \) and \( \bar{\mu} = 25 \) and 35 is used. The convergence condition is that the temperature in each layer does not vary within less than 1%.

Finally, we have to find the solution in which the atmosphere is in equilibrium with the underlying magma ocean at its bottom. The ground pressure \( P_g \) and molar fractions \( x_A \) are
functions of the ground temperature $T_g$ (see Section 2). From Equations (12) and (13), the magma being assumed to be a blackbody, $T_g$, is given as

$$
\sigma T_g^4 = F_0 + \int_0^\infty \left\{ F_{n,v}^\mu (P_x) + \mu_k F_v^e e^{-\tau_{g,0}\mu_s} \right\} d\nu,
$$

where $\sigma$ is the Stefan–Boltzmann constant ($= 5.67 \times 10^{-8} \text{W m}^{-2} \text{K}^{-4}$) and $\tau_{g,0}$ is the total optical depth of the atmosphere. We calculate $T_g$ from Equation (15) and then calculate $P_x$ and $x_A$. The gas chemical equilibrium composition in each layer, $x_A$, is obtained by interpolating linearly the tabulated data made by the NASA CEA code. The grids are prepared for $T = 2000, 2500, 3000, 3500, 4000$, and $4500$ K, $\log (P/\text{bar}) = -1, -2, -3, -4, -5, -6, -7,$ and $-8$, and $T_g$ being every $1$ K from $1500$ to $3000$ K. The convergence condition is that $T_g$ and the temperature in each layer do not vary within less than $1\%$.

Figure 4 shows the calculated temperature profiles for different substellar-equilibrium temperatures defined by

$$
T^4 = \left( 1 - A_p \right) \frac{R^2}{D^2} T_*^4,
$$

where $R_*$ and $T_*$ are, respectively, the radius and temperature of the host star, $A_p$ is the planetary albedo, and $D$ is the orbital distance of the planet. Five values of $T_{eq}$ are chosen: $T_{eq} = 1800$ K (black), $2000$ K (cyan), $2300$ K (blue), $2500$ K (green), and $3000$ K (red) (see Equation (16); $A_p = 0$). The host star is assumed to be a Sun-like star with radius of $1 \text{R}_\odot$ and effective temperature of $6000$ K and emit the blackbody radiation of $6000$ K. The solid lines show the dayside-averaged profiles (i.e., the cosine of the stellar-light zenith angle $\mu_s = 1/2$; see Equation (12)). The open circles show the temperatures at the bottom of the atmosphere, $T_b$, and the filled circles show the temperatures at the ground, $T_g$. The orange dotted line represents the total vapor pressure for the BSE composition, which corresponds to the ground.

The most remarkable feature of the temperature profiles in Figure 4 is the thermal inversion structure in the cases of $T_{eq} \geq 2300$ K. As found in Section 3, the absorption is more significant in the UV and visible wavelength regions ($0.1 \text{ to } \sim 1 \mu m$) than in the IR region ($\sim 1-4 \mu m$), mainly because of the strong UV-ray absorption by SiO and visible-light absorption by the doublet lines of Na and K. (Note that most of the absorption lines of Fe, Na, and K are too narrow to contribute to the mean opacity.) This means that the absorption of the incident stellar radiation is stronger compared to the intrinsic planetary radiation, which results in thermal inversion for $P \geq 10^{-5}$ bars. For $P \leq 10^{-5}$ bars, the temperature decreases with decreasing pressure, because the dissociation of SiO occurs as shown in Figure 5, so that the UV-ray absorption by SiO becomes weak.

As $T_{eq}$ increases, not only does the thermal inversion region extend, but $T_g$ increases. In the case of $T_{eq} = 3000$ K, $T_g$ is significantly smaller than $\mu_s^{1/4} T_{eq}$. In contrast, $T_g \simeq \mu_s^{1/4} T_{eq}$ for low $T_{eq}$, because the atmosphere is so optically thin that the ground is directly heated by stellar irradiation. In the cases of $T_{eq} \leq 2000$ K, the atmosphere is thus isothermal. Note that jumps in temperature between $T_b$ and $T_g$ are found in Figure 4. This is because those atmospheres are optically thin for the incident stellar flux and any heat transfer process except radiative transfer is not taken into account. Thus, in reality, the atmosphere is not exactly isothermal, because there should be a conductive region with steep temperature gradient near the ground. Such structure, however, has little impact on the emission spectra that we use when discussing the detectability of HSREs in secondary eclipse (see Section 5).

5. DETECTABILITY VIA SECONDARY ECLIPSE OBSERVATION

5.1. Secondary Eclipse Depth

Here we assess the detectability of the mineral atmospheres of HSREs that we have modeled via the secondary eclipse observation. This observation enables us to infer the vertical temperature profile and composition of an exoplanetary atmosphere by obtaining planetary emission spectra. In particular, the thermal inversion structure found in Section 4 is expected to be detected.

The secondary eclipse observation measures the ratio of the planetary luminosity to the sum of the stellar and planetary luminosities. The ratio is often called the secondary eclipse depth, $\epsilon_\lambda$, which is given by

$$
\epsilon_\lambda \simeq \left( \frac{R_p}{R_*} \right)^2 \frac{F_{p,\lambda} + A_p F_{s,\lambda}}{F_{s,\lambda}},
$$

where $F_{p,\lambda}$ is the emergent stellar flux and $F_{p,\lambda}$ is the emergent planetary flux calculated as

$$
F_{p,\lambda} = \pi \int_0^\infty B_\lambda (T_\gamma) e^{-\gamma d\gamma} d\gamma.
$$

Below, as in Section 4, we assume $g = 25 \text{ m s}^{-2}$, $A_p = 0$, and blackbody stellar radiation of $6000$ K. The magma composition is assumed to be BSE. Also, we suppose an HRSE with radii of $2 R_*$ orbiting a solar analog, namely, $R_p/R_* = 0.02$. To integrate Equations (17) and (18), we consider 30,000 spectral
intervals in the wavelength range between 0.1 and 100 μm; the size of each interval logarithmically increases with wavelength. Then, as in Section 4, we calculate the arithmetic mean opacities, interpolating linearly the tabulated data. We consider only the case of $\mu^* = 1/2$, because we are interested in planetary disk averaged emission (i.e., dayside average).

Figure 6 plots the secondary eclipse depth $\epsilon_\lambda$ (and also $ll D$, $ll p$) for $T_{eq} = 1800$ K (black), 2000 K (cyan), 2300 K (blue), 2500 K (green), and 3000 K (red). Panels (a) and (b) show the spectra in the wavelength region of 0.1–100 μm and 0.3–1 μm, respectively. The secondary eclipse depth spectra for $T_{eq} = 1800$ and 2000 K exhibit only some narrow-line features of Na and K. This is mainly because the atmospheres are isothermal (see Figure 4) except for the temperature jump above the ground. The line features are, thus, due to the emission from parts of the atmosphere with temperatures higher than $T_g$, while the continuous spectra are the blackbody spectra of $T_g$.

By contrast, the spectra for $T_{eq} = 2300$ and 2500 K present noticeable features of SiO around 10 and 100 μm, in addition to hundreds of narrow features of Na and K. For $T_{eq} = 3000$ K, a spectral feature by SiO around 4 μm appears in addition to those around 10 and 100 μm, as shown in the inset of Figure 6(a). The features of SiO become stronger as $T_{eq}$ increases, because the SiO abundance is sensitive to temperature and also the thermal inversion is more significant at higher temperature. Additionally, one can also identify features of the sodium doublet at 0.589 μm and the potassium doublet at 0.77 μm and narrow-line features of Fe, Na, and K in the visible band, as shown in panel (b).

5.2. Detectability

We evaluate the detectability of the mineral atmosphere of an HRSE for near-future space-based secondary eclipse observation. The photometric accuracy of the transit/eclipse observation from space depends on the instrument measurement noise, the intrinsic stellar variability, and the shot noise from photon statistics (e.g., Clanton et al. 2012). In this section, we quantify the photometric accuracy required for the line detection and discuss the feasibility, assuming the ideal case that the total noise is dominated by the shot noise (i.e., the photon-noise limit). To quantify the detectability for the photon-noise limit, we introduce the signal-to-noise ratio ($S/N$) of the detection of the secondary eclipse as

$$\text{(S/N)}_{\Delta\lambda} = \frac{N_p}{\sqrt{N_0}},$$

and

$$\simeq \frac{\epsilon_{\lambda,\Delta\lambda} \sqrt{At_{\text{obs}} R^2 \pi B_{\Delta\lambda}(T_e)}}{\mathcal{R} d^2 \hbar},$$

where $\Delta\lambda$ is the bandwidth used for the detection of the secondary eclipse, $N_0$ is the photon counts of the star, $A$ is the area of the system, $t_{\text{obs}}$ is the exposure time, $d$ is the distance of the system, $\mathcal{R}$ is the resolving power of the spectra, $\epsilon_{\lambda,\Delta\lambda}$ is the depth of the secondary eclipse within $\Delta\lambda$, $N_p$ is the
the case of $T_{eq} = 3000$ K (see Figure 7(a)), $T_{br} \simeq 3200$ K at 10 \( \mu \)m and 2700 K at 4 \( \mu \)m owing to SiO. Additionally, although not shown, $T_{br} \simeq 3500$ K at 0.6 \( \mu \)m and 0.8 \( \mu \)m (which are due to Na and K, respectively) and 3100 K at 100 \( \mu \)m (SiO). At the other wavelengths, $T_{br} \simeq T_g$ (e.g., $T_{br} = 2350$ K for $T_{eq} = 3000$ K), because the atmosphere is optically thin at those wavelengths.

Comparing the mock spectra with the blackbody spectra, one can quantify the detectability of the spectral features of Na, K, and SiO. The error bars become larger in both shorter- and longer-wavelength regions, because the number of incident photons (i.e., $B_{\Delta \lambda}(T_a)$) is small in such wavelength regions. Also, the values of $\mathcal{R}$, which are assumed to be 100 in 0.1–1 \( \mu \)m and 10 in 1–100 \( \mu \)m, affect the value of $(S/N)_{\Delta \lambda}$. As shown in Figure 7(a), the spectral features of SiO are sufficiently detectable at 4, 10, and 100 \( \mu \)m for $T_{eq} = 3000$ K. The SiO feature is also sufficiently detectable at 10 \( \mu \)m for $T_{eq} = 2500$ K (Figure 7(b)), while the feature is marginally undetectable for $T_{eq} = 2300$ K (Figure 7(c)).

The S/N for detecting the line absorption spectral feature of the secondary eclipse depth is generally smaller than that for the secondary eclipse detection. Thus, we define the secondary eclipse depth relative to 10\( \mu \)m, with $T_{eq}$, $\eta_{\lambda,\Delta \lambda}$ as

$$\eta_{\lambda,\Delta \lambda} \equiv \int_{\lambda}^{\lambda+\Delta \lambda} \frac{\epsilon_{\lambda} - \epsilon_{BB,\lambda}(T_g)}{\Delta \lambda} d\lambda,$$

(21)

where $\epsilon_{BB,\lambda}(T_g)$ is the secondary eclipse depth by the blackbody radiation with $T_g$. Using $\eta_{\lambda,\Delta \lambda}$, we estimate the detectability of the line spectral features. From Equations (20) and (21), we introduce a new quality, $(S/N)_{L,\lambda,\Delta \lambda}$, which is defined as

$$(S/N)_{L,\lambda,\Delta \lambda} = \eta_{\lambda,\Delta \lambda}(S/N)_{\Delta \lambda}.$$

(22)

When $(S/N)_{L,\lambda,\Delta \lambda}$ is sufficiently large, we can detect the line spectral feature of the secondary eclipse depth. Thus, if the minimum value of $(S/N)_{L,\lambda,\Delta \lambda}$ required to detect a line spectral feature, $|\langle S/N\rangle_{L,\lambda,\Delta \lambda}|_{\min}$, is 3, $(S/N)_{\Delta \lambda} \geq 3/\eta_{\lambda,\Delta \lambda}$ is required to do so.

Figure 8(a) shows $\eta_{\lambda,\Delta \lambda}$ for $T_{eq} = 3000$ K (red), 2500 K (green), and 2300 K (blue) with $\mathcal{R} = 100$ in 0.3–1 \( \mu \)m and 10 in 1–100 \( \mu \)m. As shown in Figure 8(a), $\eta_{\lambda,\Delta \lambda}$ takes large values at some wavelengths, because of the strong line features: $\eta_{\lambda,\Delta \lambda} \sim 1$ at 0.6 \( \mu \)m (Na) and ~0.35 at 10 \( \mu \)m (SiO) for $T_{eq} = 3000$ K (red). $\eta_{\lambda,\Delta \lambda}$ is large at ~4 \( \mu \)m because of the SiO feature peak only for $T_{eq} = 3000$ K (red), since the SiO feature is weaker than Na and K features for $T_{eq} = 2300$ and 2500 K. Also, Figure 8(b) shows $|\langle S/N\rangle_{L,\lambda,\Delta \lambda,\min}|(\equiv |\langle S/N\rangle_{L,\lambda,\Delta \lambda,\min}|_{\min})$ for $T_{eq} = 3000$ K (red), 2500 K (green), and 2300 K (blue), assuming $|\langle S/N\rangle_{L,\lambda,\Delta \lambda,\min}| = 3$ as a minimum fiducial value to detect the line spectral feature with $\mathcal{R} = 100$ in 0.3–1 \( \mu \)m and 10 in 1–100 \( \mu \)m. We obtain that $|\langle S/N\rangle_{L,\lambda,\Delta \lambda,\min}| \leq 100$ around 4, 10, and 100 \( \mu \)m; for example, $|\langle S/N\rangle_{L,\lambda,\Delta \lambda,\min}| \sim 60$ at 10 \( \mu \)m for $T_{eq} = 2300$ K (blue) and $|\langle S/N\rangle_{L,\lambda,\Delta \lambda,\min}| \sim 10$ at 4 \( \mu \)m for $T_{eq} = 3000$ K (red). Thus, observation of an HRSE in secondary eclipse can detect the components of the mineral atmosphere such as Na, K, and SiO, provided that its S/N is larger than $|\langle S/N\rangle_{L,\lambda,\Delta \lambda,\min}|$. 

Figure 6. Predicted dayside-averaged emission spectra of a hot rocky super-Earth of 2 $R_{\oplus}$ in secondary eclipse that has a mineral atmosphere in equilibrium with an underlying BSE magma ocean. The secondary eclipse depth (see Equation (17)) is shown as a function of wavelength in the range of (a) 0.1–100 \( \mu \)m and (b) 0.3–1 \( \mu \)m. The inset in panel (a) is an enlarged view of the spectra in 3–5 \( \mu \)m. Five equilibrium temperatures are chosen: $T_{eq} = 1800$ K (black), 2000 K (cyan), 2300 K (blue), 2500 K (green), and 3000 K (red). The corresponding atmospheric structures are shown by dashed lines in Figure 4. The host star is assumed to be a Sun-like star with radius of 1 $R_{\odot}$, i.e., the planetary/stellar radius ratio being 0.02) and emitting a blackbody radiation of 6000 K.

As demonstrated in Figure 7, the spectral features of Na, K, and SiO are represented by the blackbody spectra with different temperatures (i.e., brightness temperature $T_{eq}$). For example, in

| Temperature | Effective Temperature of the Atmosphere | The Astrophysical Journal, 801:144 (15pp), 2015 March 10 |
|-------------|----------------------------------------|--------------------------------------------------|
| 1800 K      | $T_{eq}$ = 1800 K                      | (black)                                           |
| 2000 K      | $T_{eq}$ = 2000 K                      | (cyan)                                            |
| 2300 K      | $T_{eq}$ = 2300 K                      | (blue)                                            |
| 2500 K      | $T_{eq}$ = 2500 K                      | (green)                                           |
| 3000 K      | $T_{eq}$ = 3000 K                      | (red)                                             |

The blackbody spectra are calculated from Equation (17) with the assumption $F_{\lambda,\Delta \lambda} = B_{\lambda}(T)$. As demonstrated in Figure 7, the spectral features of Na, K, and SiO are represented by the blackbody spectra with different temperatures (i.e., brightness temperature $T_{eq}$). For example, in
Finally, we estimate the limiting distance \( d_{\text{max}} \) interior to which an HRSE with the mineral atmosphere is detectable with a given \( |(S/N)_{\lambda} \text{min} | \), for the photon-noise limiting case. From Equation (20), \( d_{\text{max}} \) is written as

\[
\begin{aligned}
d_{\text{max}} &= \left( \frac{(S/N)_{\lambda}}{|(S/N)_{\lambda} \text{min} |} \right) \times \frac{\epsilon_{\lambda,\Delta \lambda}}{\epsilon_{\lambda,\Delta \lambda}} \frac{A_{\text{obs}} \pi B_{\lambda}(T_{\ast}) R_{\ast}}{R_{\ast}} \ R_{\ast}.
\end{aligned}
\]

Equation (20) shows \( d_{\text{max}} \) as a function of wavelength for \( |(S/N)_{\lambda} \text{min} | = 3/ \epsilon_{\lambda,\Delta \lambda} \) (i.e., the minimum S/N for the detection of line spectral features within secondary eclipse depth; shown by solid lines) or 3 (i.e., the minimum S/N for the detection of the secondary eclipse depth itself; shown by dotted lines); \( R_{\ast} = R_{\ast} \), \( R_{\ast} = 0.02 R_{\ast} \), \( A = \pi (5\text{m}/2)^2 \), \( t_{\text{obs}} = 10 \text{hr} \), and \( R_{\ast} = 100 \text{ in } 0.3-1 \mu \text{m and } 10 \text{ in } 1-100 \mu \text{m} \), and \( d = 100 \text{ pc} \) (see the text for details). The corresponding atmospheric structures are shown by dashed lines in Figure 4.

Figure 9 shows \( d_{\text{max}} \) around 4 \( \mu \text{m} \) is not shown for \( T_{\text{eq}} = 2300 \) and 2500 K, because the Na, K, and SiO features in those cases are indistinguishable from each other when integrating the secondary eclipse depth with respect to wavelength with \( R_{\ast} = 10 \).
Assuming line spectral features within secondary eclipse depth around 4, 10, and 100 wavelengths for three equilibrium temperatures \( T = 2300 \text{ K} \), \( 2500 \text{ K} \), and \( 3000 \text{ K} \), the corresponding atmospheric structure is shown in Figure 4. The solid lines show the limiting distance \( d_{\text{max}} \) to detect the line spectral features within secondary eclipse depth around 4, 10, and 100 \( \mu \text{m} \), assuming \((\text{S/N})_{\Delta \lambda} = 3/\eta_1 \) shown in Figure 8(b). The dotted lines show the limiting distance \( d_{\text{max}} \) to detect the secondary eclipse depth itself, assuming \((\text{S/N})_{\Delta \lambda} = 3 \). The host star is assumed to be a Sun-like star with radius of 1 \( R_{\odot} \) (i.e., the planetary/stellar radius ratio being 0.02) and emitting a blackbody radiation of 6000 K.

Table 2 summarizes \( d_{\text{max}} \) for the SiO detection. The limiting distance \( d_{\text{max}} \) increases with increasing \( T_{\text{eq}} \); because an HRSE with higher \( T_{\text{eq}} \) shows greater planetary emission and a more remarkable line absorption spectral feature of the secondary eclipse depths. Thus, the mineral atmospheres of more distant HRSEs would be also detectable if they have higher \( T_{\text{eq}} \).

### 5.3. Application to Known HRSEs

We show the simulated secondary eclipse depth spectra of four known close-in super-Earths, CoRoT-7b, Kepler-10b, Kepler-78b, and 55 Cnc e, in Figure 10. Within the 1\( \sigma \) errors of their observed masses and radii, it is possible that those super-Earths are naked rocky planets. Note that, according to Dragomir et al. (2014), the 1\( \sigma \) upper limit on the measured 55 Cnc e’s density just reaches the pure rock regime. If so, they have mineral atmospheres, because of high \( T_{\text{eq}} \) (see Table 3). In the simulations, we have assumed \( \Omega = 10 \) in 1–100 \( \mu \text{m} \) and 100 in 0.3–1 \( \mu \text{m} \). The values of the planetary and stellar parameters that we have used are listed in Table 3.

The secondary eclipse depth becomes large as \( R_p/R_* \) increases and \( T_{\text{eq}} \) increases. Thus, the secondary eclipse depth of 55 Cnc e \( (R_p/R_* = 2.12, R_p/R_* = 1.39) \) is largest, while that of Kepler-10b \( (R_p/R_* = 1.39 R_p/R_* = 0.77) \) is smallest. Despite its larger \( R_p/R_* \), the secondary eclipse depth of CoRoT-7b is smaller than that of Kepler-78b, because \( T_{\text{eq}} \) of CoRoT-7b is smaller than that of Kepler-78b.

Prominent absorption features are found around \( \lambda = 0.6 \mu \text{m} \) (Na), 0.77 \( \mu \text{m} \) (K), 4 \( \mu \text{m} \), 10 \( \mu \text{m} \), and 100 \( \mu \text{m} \) (SiO). In particular, in the cases of Kepler-10b and 55 Cnc e, those features would be detectable by the near-future space-based observation that we have assumed in Section 5.2, because the distances of these systems are shorter than \( (R_p/R_*)^{-1} (R_p/R_*)^{-2} \) \( d_{\text{max}} \) from Equations (17) and (23).

Demory et al. (2012) have already reported the detection of the secondary eclipse depth of 55 Cnc e with the Spitzer Space Telescope at 4.5 \( \mu \text{m} \). The measured brightness temperature of 2360 ± 300 K is consistent with our result shown in Figure 10(d), although the error is large. Also, the SiO IR-absorption features of an HRSE that is brighter and closer than 55 Cnc e would be detectable with Spitzer in the IRAC 4.5 and 8 \( \mu \text{m} \) channel.

Using Equations (20) and (21), we define the line contrast to the total flux, \( C_{\text{L}(\lambda,\Delta \lambda)} \), as

\[
C_{\text{L}(\lambda,\Delta \lambda)} \equiv \eta_{\lambda,\Delta \lambda} \epsilon_{\lambda,\Delta \lambda}.
\]

The photometric accuracy should be smaller than \( C_{\text{L}(\lambda,\Delta \lambda)} \) in order to detect the line spectra feature of the secondary eclipse depth. There are several proposed missions that aim to characterize transiting exoplanets, such as Fast Infrared Exoplanet Spectroscopy Survey Explorer (FINESSE; e.g., Deroo et al. 2012) and the Exoplanet Characterization Observatory (EChO; e.g., Tinetti et al. 2012). Here we compare our results with the accuracy of EChO. Figure 11 shows the theoretical (solid line) and mock-EChO (bars) secondary eclipse depth spectra for a super-Earth with a mineral atmosphere, using 55 Cnc e’s parameters. Then, we create the mock-EChO spectra with \( \Omega = 50 \) in 1–5 \( \mu \text{m} \) and 30 in 5–16 \( \mu \text{m} \), and the photometric accuracy of EChO in Chemical census mode (Waldmann & Pascale 2014). Our result demonstrates that EChO has enough accuracy to detect the SiO feature of the mineral atmosphere of 55 Cnc e around 4 and 10 \( \mu \text{m} \).

Table 4 shows the line contrasts \( C_{\text{L}} \) of Na (0.59 \( \mu \text{m} \), K (0.77 \( \mu \text{m} \), and SiO (4, 10 and 100 \( \mu \text{m} \) for \( T_{\text{eq}} = 2300, 2500, \) and \( 3000 \text{ K} \) (\( \Omega = 100 \) for \( \lambda \leq 1 \mu \text{m} \) and \( \Omega = 10 \) for \( \lambda \geq 1 \mu \text{m} \)) and 55 Cnc e’s parameters (\( \Omega = 100 \) for \( \lambda \leq 1 \mu \text{m} \), \( \Omega = 50 \) for \( 1 \mu \text{m} \leq \lambda \leq 5 \mu \text{m} \), and \( \Omega = 30 \) for \( \lambda \geq 5 \mu \text{m} \)). The photometric accuracy of EChO in Chemical census mode of 55 Cnc e (Waldmann & Pascale 2014) is also shown in Table 4. Note that the values of \( C_{\text{L}} \) at 4 \( \mu \text{m} \) are not shown for \( T_{\text{eq}} = 2300 \) and 2500 K, because the Na, K, and SiO features in those cases are indistinguishable with \( \Omega = 10 \). We obtain that \( C_{\text{L}(\lambda,\Delta \lambda)} \geq 10 \text{ ppm} \) for Na (0.59 \( \mu \text{m} \), K (0.77 \( \mu \text{m} \), and SiO (4, 10, and 100 \( \mu \text{m} \)); for example, \( C_{\text{L}(\lambda,\Delta \lambda)} \sim 14 \text{ ppm} \) at 0.77 \( \mu \text{m} \) and 24 ppm at 10 \( \mu \text{m} \) for \( T_{\text{eq}} = 2500 \text{ K} \), and \( C_{\text{L}(\lambda,\Delta \lambda)} \sim 26 \text{ ppm} \) at 0.59 \( \mu \text{m} \), 34 ppm at 0.77 \( \mu \text{m} \), and 67 ppm at 10 \( \mu \text{m} \) for \( T_{\text{eq}} = 3000 \text{ K} \). The required photometric accuracy to detect the SiO features at 4 and 10 \( \mu \text{m} \) is achievable with the Chemical Census mode of EChO for 55 Cnc e.

---

\( ^3 \) Waldmann & Pascale (2014) showed the simulated EChO observation of 55 Cnc e assuming a CO\(_2\) and H\(_2\)O atmosphere model. We use the noise level assumed in their Figure 9 because the depth of their spectra is similar to ours.
orbiting stars with days. Fressin et al. (2013) have estimated \( N = \frac{2}{3} \) in 0.3–1 \( \mu \)m and 10 in 1–100 \( \mu \)m and the planets’ parameters shown in Table 3.

### Table 3: Assumed Planetary and Stellar Parameters

| Parameter | Corot-7b | Kepler-10b | Kepler-78b | 55 Cnc e |
|-----------|----------|------------|------------|---------|
| \( M_p \) | 7.42 \( M_\oplus \) | 3.33 \( M_\oplus \) | 1.69 \( M_\oplus \) | 8.09 \( M_\oplus \) |
| \( R_p \) | 1.58 \( R_\oplus \) | 1.47 \( R_\oplus \) | 1.20 \( R_\oplus \) | 1.99 \( R_\oplus \) |
| \( D \) | 0.0172 AU | 0.0168 AU | 0.0092 AU | 0.0155 AU |
| \( T_{eq} \) | 2550 K | 3090 K | 3000 K | 2700 K |
| \( R_* \) | 0.82 \( R_\odot \) | 1.06 \( R_\odot \) | 0.74 \( R_\odot \) | 0.94 \( R_\odot \) |
| \( T_* \) | 5250 K | 5700 K | 5200 K | 5200 K |
| Distance | 150 pc | 173 pc | ... | 12.3 pc |

\( ^a \) Hatzes et al. (2011); \( ^b \) Bruntt et al. (2010); \( ^c \) Léger et al. (2009).
\( ^d \) Dumusque et al. (2014); Fressin et al. (2011).
\( ^e \) Howard et al. (2013).
\( ^f \) Dragoni et al. (2014); Nelson et al. (2014); Ehrenreich et al. (2012).

#### 5.4. How Many HRSEs Are Detectable via Near-future Observation?

The Kepler space telescope has discovered 4250 planet candidates (as of 2014 November 30; http://exoplanets.org). The Kepler Objects of Interest (KOIs) include super-Earth-size objects with short periods (i.e., HRSEs), in particular, 751 objects with \( R_p \leq 2 R_\oplus \) orbiting stars with \( T_{\text{eff}} = 5300–6000 \) K. Among them, there are 60 KOIs with \( T_{eq} \geq 2300 \) K. If they are naked rocky planets, their mineral atmospheres can be identified by secondary eclipse observations with sufficient S/Ns. We estimate the expected number of such HRSEs detectable by near-future observations.

Assuming a uniform distribution of G-type stars, the number of the detectable HRSEs, \( \bar{N}_{\text{HRSE}} \), is given by

\[
\bar{N}_{\text{HRSE}} \approx r N_G \frac{4\pi}{3} d_{\text{max}} \left[ \frac{(S/N)_{\Delta\lambda}}{\eta_{\lambda};\Delta\lambda} \right]^3,
\]

where \( r \) is the occurrence rate of HRSEs with \( T_{eq} \geq 2300 \) K hosted by G-type stars and \( N_G \) is the number density of G-type stars. The HRSEs with \( T_{eq} \geq 2300 \) K, which should exhibit the prominent emission features (Figure 7), correspond to planets with period \( P \lesssim 2 \) days around G-type stars. Fressin et al. (2013) estimated, using KOI host stars, the occurrence rate of planets with \( 1.25 R_{\oplus} \leq R_p \leq 2 R_{\oplus} \) hosted by G-type stars to be close to 0.35. They also estimated the occurrence rate of planets with \( 1.25 R_{\oplus} \leq R_p < 2 R_{\oplus} \) and \( 0.8 < P < 2 \) days to be \((1.7 \pm 0.3) \times 10^{-3}\). Using their results, the occurrence rate of the planets with \( 1.25 R_{\oplus} \leq R_p < 2 R_{\oplus} \) and \( 0.8 < P < 2 \) days hosted by G-type stars is estimated to be \( r \approx 6 \times 10^{-4} \). Here we use \( r = 6 \times 10^{-4} \) as a fiducial value of the occurrence rate.

In Section 5.2, we estimated \( d_{\text{max}} \left[ \frac{(S/N)_{\Delta\lambda}}{\eta_{\lambda};\Delta\lambda} \right] \) to be 430 pc (\( T_{eq} = 3000 \) K), 150 pc (\( T_{eq} = 2500 \) K), and 30 pc (\( T_{eq} = 2300 \) K) for 10\(^{-4}\) observation (see Figure 9 and Table 2). These HRSEs with \( T_{eq} = 2300, 2500, \) and 3000 K have orbital periods \( P \approx 0.93, 1.6, \) and 2.0 days, respectively. Hence, we take the simple mean \[ (430^3 + 150^3 + 30^3)/3 \] to be 300 pc as a fiducial value of the limiting distance for HRSEs with \( 0.8 < P < 2 \) days. Inputting \( r = 6 \times 10^{-4} \) and \( N_G \approx 6 \times 10^{-3} \) pc\(^{-3}\) (see a recent review by Traub & Oppenheimer 2011, pp. 111–156) in Equation (25), we find that within 300pc there are approximately 400 HRSEs whose 10\(^{-4}\) features are detectable. Taking the transiting probability of \( \sim 0.2 \) (\( \sim R_p/D \) for \( P = 1.3 \) days) into account, one will be able to detect the 10\(^{-4}\) features from \( \sim 80 \) transiting HRSEs by a 5 m space telescope equipped with a photon-noise-limited instrument.
6. MODEL VALIDATION AND FUTURE STUDY

6.1. Scattering

In this study, we have ignored the effect of scattering on the thermal structure of the mineral atmosphere. There are two possible sources for scattering. One is Rayleigh scattering by the major gases. The cross section for Rayleigh scattering by gas species $A$, $\sigma_{\text{Ray}}^A$, ignoring the polarizability anisotropy, is approximately given as (e.g., CRC Handbook 2011)

$$\sigma_{\text{Ray}}^A = \frac{8\pi}{3c^4}(2\pi\nu)^4\alpha^2_A,$$  \hspace{1cm} (26)

where $\alpha_A$ is the static average electric dipole polarizability of gas species $A$. According to CRC Handbook (2011), $\alpha_A$ for ground-state atoms and diatomic molecules in the unit of $10^{-24} \text{ cm}^3$ are 24.11 for Na, 43.4 for K, 0.802 for O, and 1.5689 for O$_2$. While $\alpha_A$ for SiO is unavailable in the literature, to our knowledge, it should not differ by several orders of magnitude from those of the other gases. Comparing the cross sections for Rayleigh scattering by those gases with the total absorption cross section calculated in Section 3, we have confirmed that the former are smaller by several orders of magnitude than the latter in most of the wavelength region of interest, except for the narrow ranges between 0.1 and 0.15 $\mu$m and between 0.3 and 0.45 $\mu$m. We have integrated the thermal structure incorporating the effect of the Rayleigh scattering by Na, which results in only a few percent difference in temperature. Also, the Rayleigh and Mie scattering by cloud particles can affect the thermal structure of the mineral atmosphere, if present. However, since the atmospheric temperature is always higher than the vapor pressure of rock, as shown in Figure 4, no condensation cloud is formed in the atmosphere.

6.2. Non-LTE Effect

The approximation of LTE is invalid at low pressures. In this study, we have considered a pressure range of $1\times10^{-8}$ bars. For LTE to be attained, thermalization due to atomic/molecular collisions must occur faster than radiative cooling. The collisional timescale, $\tau_{\text{coll}}$, is $\sim kT/(P\sigma_{\text{coll}}v)$, where $\sigma_{\text{coll}}$ and $v$ are the collisional cross section and thermal velocity of molecules. For SiO, since $\sigma_{\text{coll}} \approx 3 \times 10^{-15} \text{ cm}^2$, $T \approx 3000 \text{ K}$, $v \approx 8 \times 10^4 \text{ cm} \text{s}^{-1}$, and the typical radiative cooling timescale (i.e., the typical lifetime of excited states) $\tau_{\text{cool}} \approx 1 \times 10^{-2} \text{ s}$ (Barton et al. 2013), LTE is valid for $P \gtrsim 2 \times 10^{-7}$ bars. Since the emission from the low-pressure region of $P \lesssim 2 \times 10^{-7}$ bars makes little contribution to the secondary eclipse depth, the LTE approximation is valid for the SiO-dominated atmosphere of special interest in this study.

6.3. Photodissociation of SiO

Our equilibrium calculations show that the major gas species in the mineral atmosphere are Na, K, Fe, O, O$_2$, Si, and SiO (Section 4). Although having been ignored in this study, photodissociation of SiO would occur in such an atmosphere by irradiation of stellar UV (e.g., Vorypaev 1981).

Jolicard et al. (1997) provided the photodissociation cross section of SiO, $\sigma_{\text{dis}}$, in the wavelength range between 0.153 and 0.157 $\mu$m, where the cross section decreases monotonically with increasing wavelength from $\sim 10^{-17}$ to $10^{-19} \text{ cm}^2$. The energy of UV rays of $\lambda > 0.157 \mu$m is not high enough to dissociate SiO significantly; instead, the electron transition of SiO is dominant, as discussed in Section 3. Also, for $\lambda = 0.152–0.163 \mu$m, the electron-transition cross section of Si is larger than $10^{-17} \text{ cm}^2$ and thus larger than $\sigma_{\text{dis}}$. Therefore, it is the UV ray of $\lambda \lesssim 0.152 \mu$m that dissociates SiO efficiently in the mineral atmosphere. Although no other published data for $\sigma_{\text{dis}}$ are available, $\sigma_{\text{dis}}$ is unlikely to decrease with decreasing wavelength. Below, we make a rough estimate of the impact of SiO photodissociation on the atmospheric structure and the emission features.

Using $\sigma_{\text{dis}} > 1 \times 10^{-17} \text{ cm}^2$ with $x_{\text{SiO}} = 1 \times 10^{-3}$, $\mu = 20$, and $g = 2500 \text{ cm} \text{s}^{-2}$, we calculate the SiO photodissociation optical depth, which is defined by

$$\tau_{\text{dis}} = \frac{x_{\text{SiO}}\sigma_{\text{dis}}}{\mu m_\text{H}^2}P,$$  \hspace{1cm} (27)

where $m_\text{H}$ is the proton mass. Then, we find that $\tau_{\text{dis}} = 1$ at $P < 8 \times 10^{-8}$ bars. This means that the atmospheric structure for $P \gtrsim 8 \times 10^{-6}$ bars is affected significantly by photodissociation of SiO. Since the emission features shown in Figure 4 arise from the region of $P \gtrsim 3 \times 10^{-3}$ bars (see Figure 6), the emission spectra are unlikely to be affected by the photodissociation. More detailed examination requires photochemical calculations done consistently with radiative transfer calculations, which must be a future study.

6.4. Tidal Heating

Our atmospheric models do not include the effect of tidal heating, described in Section 4 ($F_0 = 10$ W m$^{-2}$ being assumed). According to Henning et al. (2009), tidal heating dominates stellar irradiation under somewhat extreme circumstances such that the planetary eccentricity, $e$, is larger than 0.1 and the orbital period is less than 2 days. Also, Miguel et al. (2011) showed that addition of tidal heating hardly changes the surface temperature of HRSEs for $e = 0.01$ and 0.001 and the quality factor of the planet, $Q$, of 200 and 20,000. Indeed, although not shown, we have confirmed that there is no significant change in the atmospheric structure for $T_{\text{eq}} = 3000 \text{ K}$, by calculating the temperature profiles with
\[ F_0 = 10^3 - 10^7 \text{ W m}^{-2}, \] being equivalent to tidal heat flux for \( e = 0.01 \) and 0.001 and \( Q = 200 \) and 20,000.

### 6.5. Temperature Jump at the Bottom

Allowing the temperature jump would affect the composition of the atmosphere. If we included the thermal conduction, we would have no temperature jump at the bottom in the atmosphere, and we would have higher \( T_g \) and a thicker atmosphere than our model in this study, which is more detectable. The HRSE atmosphere is thin enough for radiation to heat the atmosphere more effectively than thermal conduction. Thus, although the thermal conduction would change \( T_g \) and thus the composition of the atmosphere, it would be ineffective in changing the emission spectra of HRSEs.

### 6.6. Impact of Potassium on Thermal Structure and Detectability

As shown in Section 2, our chemical equilibrium calculations yield much more abundant potassium than Schaefer \& Fegley (2009) did. Although not shown, we have confirmed that such difference in K abundance has only a small impact on the thermal structure of the atmosphere: our calculations have demonstrated that the maximum differences in temperature are \( \sim 2.86 \), \( \sim 2.27 \), and \( \sim 1.89\% \) for \( T_{eq} = 3000 \), 2500, and 2300 K, respectively. Thus, the secondary eclipse depths in the IR region are hardly affected.

A direct impact on the secondary eclipse depth is found at \( \lambda = 0.77 \mu\text{m} \). Detecting potassium may be useful for constraining the magma composition, because the potassium abundance is different by one order of magnitude from MORB to the upper crust, as shown in Figure 2.

### 6.7. Other Observation Methods to Detect Mineral Atmospheres

Other observation methods for atmospheres of close-in exoplanets include transmission spectroscopy and planetary radial velocity (PRV) measurement, in addition to secondary eclipse observation. It would, however, be difficult to detect the HRSEs’ atmospheres via transmission spectroscopy of the planetary disk because of their small scale height. The part of the HRSE’s atmosphere observed by transmission spectroscopy is the rim where horizontal heat and composition transport between the dayside and nightside would be important. The examination requires 3D calculations of atmospheric circulation done consistently with radiative transfer calculations, which must be a future study.

Recently, several molecules in the dayside spectra of hot Jupiters have been successfully detected using the high dispersion spectrograph (Brogi et al. 2012; Rodler et al. 2012; Birkby et al. 2013; de Kok et al. 2013; Rodler et al. 2013; Lockwood et al. 2014). This method utilizes the cross-correlation analysis of the spectra and the model template and directly detects PRV. Here we estimate the feasibility of the PRV detection of the mineral atmosphere of HRSEs. For the most optimistic case, the S/N of the PRV is determined by the photon noise,

\[
\text{(S/N)}_{\text{PRV}} = \sqrt{\frac{N_{\text{line}}}{e_{\text{sat}}}} \text{(S/N)}_{\Delta \lambda} C_{L(\lambda, \Delta \lambda)},
\]

where \( N_{\text{line}} \) is the effective number of molecular lines available for the detection and \( \zeta \) is the total efficiency of the high-dispersion instrument (see Kawahara et al. 2014). Although the determination of the precise value of \( N_{\text{line}} \) requires full simulations of the spectra including the terrestrial transmission and the night airglow, we here perform a 1st-order-of-magnitude estimate of the detectability of the Na and K lines, assuming a 30 m-class ground-based telescope.

The number of Na and K lines within the secondary eclipse depth spectrum of an HRSE for \( T_{eq} \geq 2300 \text{ K} \), \( N_{\text{line}} \), is \( \sim 100 \); the line contrast, \( C_{L(\lambda, \Delta \lambda)} \), is \( \sim 0.5 \); and the mean value of those depths, \( \epsilon_{\lambda} \), is \( \sim 10^{-4} \), in the IR wavelength region (1–10 \( \mu\text{m} \)), as shown in Figure 6. The resolving power of the instrument, \( \mathcal{R} \), is required to be large enough to resolve those Na and K lines. To know this value of \( \mathcal{R} \), we have reintegrated the secondary eclipse depth for \( T_{eq} = 2500 \text{ K} \) around several Na and K line peaks in the IR wavelength region (3.70–3.75 \( \mu\text{m} \)) by line-by-line calculation. We have confirmed that \( \mathcal{R} = 10^5 \) is enough to resolve the Na and K lines. Thus, we use \( \mathcal{R} = 10^5 \) below as a fiducial value of \( \mathcal{R} \). From Equation (25), the distance of the system within which at least one transiting HRSE exists is \( \sim 70 \text{ pc} \). Assuming a 30 m telescope with \( \zeta = 0.1 \), we obtain the expected S/N for detecting the Na and K lines,

\[
\text{(S/N)}_{\text{PRV}} \sim 8 \left( \frac{\epsilon_{\lambda}}{10^{-4}} \right) \left( \frac{70 \text{ pc}}{10^4 \text{ pc}} \right) \left( \frac{R_g}{1 \text{ R}_\oplus} \right) \left( \frac{C_{L(\lambda, \Delta \lambda)}}{0.5} \right) \left( \frac{A}{100} \right) \left( \frac{0.1 \pi \lambda^2}{10^5} \right) \left( \frac{10^5 \mathcal{R}}{10^2} \right) \left( \frac{10^2 \text{ m}^2}{10^2 \text{ m}^2} \right) \left( \frac{10 \text{ hr}}{10 \text{ hr}} \right) \left( \frac{\pi B(T_g)/h}{\mathcal{R}} \right),
\]

where \( 10^{-26} \text{ m}^2 \text{s}^{-1} \) corresponds to the mean value of \( \pi B(T_g)/h \) in the wavelength region between 1 and 10 \( \mu\text{m} \), assuming \( T_g = 6000 \text{ K} \). This order-of-magnitude estimate suggests that it would be possible to detect Na and K in the HRSEs’ atmospheres via PRV measurement in the very large telescope era.

### 7. SUMMARY AND CONCLUSIONS

In this study, we have examined the detectability of HRSEs that have atmospheres in the gas/melt equilibrium with the underlying magma ocean via secondary eclipse observations. First, we have performed gas-melt equilibrium calculations and showed that the major atmospheric species are Na, K, Fe, SiO, O, and O2 (Section 2). We have called this atmosphere the mineral atmosphere in this study.

Second, for those species, we have compiled the absorption-line data available in the literature and calculated their absorption opacities in the wavelength region of 0.1–100 \( \mu\text{m} \) (Section 3). We have found that the SiO absorption dominates in the UV and IR wavelength regions, while strong absorption by Na and K is found in the visible region. In this atmospheric gas, the opacity is larger in the UV and visible regions than in the IR region.

Third, using those opacities, we have integrated the thermal structure of the atmosphere (Section 4). The most important finding is that thermal inversion occurs in the atmosphere with relatively high equilibrium temperature (i.e., \( \mu_{1/4} T_{eq} \geq 1900 \text{ K} \)), because the UV and visible absorption by SiO dominates the IR absorption by SiO and others. The presence of thermal inversion has a crucial impact on the detectability via secondary eclipse observation.

Finally, by calculating the ratio of the planetary and stellar emission during secondary eclipse, we have quantified the detectability (Section 5). We have found prominent emission
features due to SiO at 4, 10, and 100 μm. Comparing our predicted spectrum with a mock spectrum we made, we have demonstrated that the mineral atmosphere of a hot rocky super-Earth of radius 2 R_E with T_{eq} = 2300 K orbiting a solar analog would be detectable by a 5 m space telescope.

The Transiting Exoplanet Survey Satellite (TESS) is a planned space telescope for NASA’s Explorer program and is dedicated to an all-sky transit survey of exoplanets (Ricker et al. 2010). It is predicted that TESS will discover more than 100 transiting Earth-sized exoplanets with short orbital periods. After discovery of nearby HRSEs, follow-up observations by satellites with large telescopes such as JWST, Spitzer, FINESSE, and EChO will open new exotic worlds of the mineral atmospheres.

We thank E. J. Barton and J. Tennyson for sharing their knowledge of SiO opacity with us. We also thank Y. Abe, K. Kurosaki, and B. Fegley Jr. for fruitful discussion. We really appreciate the anonymous referee’s careful reading and constructive comments, which have helped improved this paper greatly. This study is supported by the Challenging Research Award from the Tokyo Institute of Technology, Grants-in-aid for Scientific Research (No. 25400224 and 25800106) from the Japan Society for the Promotion of Science (JSPS) and the Astrobiology Project of the CNSI, NINS (AB261006).

APPENDIX

CALCULATION METHOD OF THE MEAN OPACITIES

In this study, we use mean opacities for simulating the atmospheric structure and emission spectra, instead of line-by-line calculations. While we integrate the line opacities of O, O_2, Na, K, and Si with wavelength resolution high enough to reproduce line profiles, we use low-resolution grids to calculate the mean opacity of SiO, because there are too many absorption lines to reproduce the line profile of SiO in a practical CPU time.

Figure A1 presents how to calculate the mean opacity of SiO when an interval between adjacent lines is less than 1 μm. When an interval between adjacent lines is smaller than 2Δν/D and 2(Γ_i + Γ_y) (see the yellow-colored region in Figure A1), we divide the interval equally into quarters. On the other hand, when an interval is larger than 2Δν/D and 2(Γ_i + Γ_y) (see the blue-colored region in Figure A1), we select a total of five grids: (ν_{0,i}, ν_{0,i+1}), the larger of (ν_{0,i} + 2Δν/D and ν_{0,i} + 2(Γ_i + Γ_y)) (≡ ν_{i,D}), the smaller of (ν_{0,i+2} ± 2Δν/D and ν_{0,i+1} ± 2(Γ_i + Γ_y)) (≡ ν_{i,L}), and a midpoint between ν_{0,i} and ν_{0,i+1} (≡ ν_{0,i}). When we integrate the line opacities around the line center, we use a trapezoidal integration method. On the other hand, when integrating line opacities between ν_{i,L} and ν_{i,D}, we approximate the integration as the sum of the areas of the shaded boxes.

When an interval is larger than 1 μm, we use the line opacities at ν_{0,i}, ν_{0,i+1}, and 50 grids between those points; those grids are selected so that the size of each interval logarithmically increases with frequency. The integration is done in the same way above.

When simulating the atmospheric thermal structure, we adopt the harmonic mean opacities. This is because the left-hand side of Equation (10) contains the Planck function B_i(T) and its right-hand side contains the opacity in the denominator of dF / dτ. On the other hand, when calculating the planetary emission spectra, we use the arithmetic mean opacities. This is because Equation (18) includes the Planck function multiplied by the exponential of the negative opacity and the opacity (i.e., B_i e^{-τ_i}(m = 1, 2, 3, ⋯)).

REFERENCES

Allard, F., Hauschildt, P. H., & Schwenke, D. 2000, ApJ, 540, 1005
Asimov, P. D., & Ghiorso, M. S. 1998, AmMin, 83, 1127
Barnes, R., Raymond, S. N., Greenberg, R., Jackson, B., & Kibr, N. A. 2010, ApJ, 709, L95
Barton, E. J., Yurchenko, S. N., & Tennyson, J. 2013, MNRS, 434, 1469
Batalha, N. M., Borucki, W. J., Bryson, S. T., et al. 2011, ApJ, 729, 27
Bean, J. L., Miller-Ricci Kempt, E., & Homeier, D. 2010, Natur, 468, 669
Birkby, J. L., de Kok, R. J., Brogi, M., et al. 2013, MNRS, 436, L35
Brogi, M., Snellen, I. A. G., de Kok, R. J., et al. 2012, Natur, 486, 502
Bruntt, H., Deetal, M., Fridlund, M., et al. 2010, A&A, 519, A51
Clampin, M. 2008, SPIE Proc., 7010, 01
Clanton, C., Beichman, C., Vasisht, G., Smith, R., & Gaudi, B. S. 2012, PASP, 124, 700
CRC Handbook of Chemistry and Physics (92nd ed.; CRC Press)

de Kok, R. J., Brogi, M., Snellen, I. A. G., et al. 2013, A&A, 554, A82
Deming, D., Harrington, J., Laughlin, G., et al. 2007, ApJL, 667, L199
Demory, B.-O., Gillon, M., Seager, S., et al. 2012, ApJL, 751, L28
Deroo, P., Swain, M. R., & Green, R. O. 2012, SPIE Proc., 8442, 41
Dragomir, D., Matthews, J. M., Winn, J. N., & Rowe, J. F. 2014, in IAU Symp. 293, ed. N. Haghighipour (Cambridge: Cambridge Univ. Press), 52
Dumusque, X., Bonomo, A. S., Haywood, R. D., et al. 2014, ApJ, 789, 154
Ehrenreich, D., Bourrier, V., Bonfinis, X., et al. 2012, A&A, 547, A18
Fegley, B., & Cameron, A. G. W. 1987, E&PSL, 82, 207
Fortney, J. J., Marley, M. S., & Barnes, J. W. 2007, ApJ, 659, 1661
Fressin, F., Torres, G., Charbonneau, D., et al. 2013, ApJ, 766, 81
Fressin, F., Torres, G., Desert, J.-M., et al. 2011, ApJS, 197, 5
Ghiorso, M. S., & Sack, R. O. 1995, CoMF, 119, 197
Gordon, S., & McBride, B. J. 1996, NASA Reference Publication 1311, http://www.gcr.nasa.gov/WWW/CEAWeb/RP-1311.pdf
Grasset, O., Schneider, J., & Sotin, C. 2009, ApJ, 693, 722
Gray, D. F. 1976, The Observation and Analysis of Stellar Photospheres (Cambridge: Cambridge Univ. Press)
Hatzes, A. P., Fridlund, M., Nachmani, G., et al. 2011, ApJ, 743, 75
Henning, W. G., O’Connell, R. J., & Sasselov, D. D. 2009, ApJ, 707, 1000
Howard, A. W., Sanchis-Ojeda, R., Marcy, G. W., et al. 2013, Natur, 503, 381
Irwin, A. W. 1981, ApJS, 45, 621
