Measurement of the forward-backward charge asymmetry and extraction of $\sin^2\theta_W$ in
$p\bar{p} \rightarrow Z/\gamma^* + X \rightarrow e^+ e^- + X$ events produced at $\sqrt{s} = 1.96$ TeV

V.M. Abazov36, B. Abbott75, M. Abolins65, B.S. Acharya29, M. Adams51, T. Adams49, E. Aguilo6, S.H. Ahn31,
M. Ahsan59, G.D. Alexeev36, G. Alkhazov69, A. Alton44a, G. Alveson62, G.A. Alves2, M. Anastassiadis35,
L.S. Ancu35, T. Andeen53, S. Anderson45, B. Andrieu17, M.S. Anzelo53, M. Aoki20, Y. Arnoud14, M. Arov60,
M. Arthaud18, A. Askev49, B. Asman41, A.C.S. Assis Jesus3, O. Atrimentov49, C. Avila8, F. Badaud13,
A. Baden61, L. Bagby50, B. Baldin50, D.V. Bandurin59, P. Banerjee29, S. Banerjee29, E. Barberis63, A.-F. Barfuss15,
P. Bargassa80, P. Baringer58, J. Barreto2, J.F. Bartlett50, U. Bassler18, D. Bauer43, S. Beale9, A. Bean58,
M. Begalli4, M. Begel73, C. Belanger-Champagne41, L. Bellantoni50, A. Bellavance39, J.A. Benitez65, S.B. Beri27,
G. Bernardi17, R. Bernhard21, I. Bertram42, M. Besançon18, R. Beuselinck43, V.A. Bezzubnov49, P.C. Bhat50,
V. Bhattachar47, C. Biscarat20, G. Blazey52, G. Blankenship43, S. Blessing49, D. Bloch19, K. Bloom67,
A. Boehrlein50, D. Boline62, T.A. Bolton59, E.E. Boos8, G. Borissov42, T. Bose77, A. Brandt78, R. Brock65,
G. Brooijmans70, A. Bross50, D. Brown1, N.J. Buchanan49, D. Buchholz53, M. Buehler81, V. Buescher22,
V. Bunichev38, S. Burdin42b, S. Burke45, T.H. Burnett82, C.P. Buszello43, J.M. Butler62, P. Caffarai29, S. Calvet16,
J. Cammin21, W. Carvalho43, B.C.K. Case50, H. Castillo-Valdez33, S. Chakraborti18, D. Chakraborty52,
K. Chan6, K.M. Chan55, A. Chandra48, F. Charles19, E. Chen45, F. Chevalier14, D.K. Cho62, S. Choi32,
B. Choudhary28, L. Christofek77, T. Christoudias47, S. Cihangir50, D. Claes67, J. Clutter58, M. Cooke80,
W.E. Cooper9, M. Corcoran80, F. Coudere18, M.-C. Cousinou55, S. Crépoin-Rauh41, D. Cutts57, M. Cwiko40,
H. da Motta2, A. Das45, G. Davies43, K. De8, S.J. de Jong35, E. De La Cruz-Burelo44, C. De Oliveira Martins3,
J.D. Degenhardt64, F. Déliot18, M. Demarteau50, R. Demma71, D. Denisov50, S.P. Denisov39, S. Desai50,
H.T. Dietel50, M. Diesburg50, A. Dominguez67, H. Dong72, L.V. Dudko38, L. Duflot16, S.R. Dugad29, D. Duggan9,
A. Dupperin15, J. Dyer69, A. Dyshliuk52, M. Eads77, D. Edmunds65, J. Ellison48, V.D. Elvira50, Y. Enari77,
S. Eno61, P. Ermolov38, H. Evans54, A. Evdokimov73, V.N. Evdokimov39, A.F. Feseropoulos59, T. Ferbel71,
F. Fiedler24, F. Filho25, W. Fisher50, H.E. Fisk50, M. Fortner32, H. Fox32, S. Fu50, S. Fuentes50, T. Gadfort70,
C.F. Galea35, E. Gallas50, A. Garcia-Bellido82, V. Garrolov37, P. Gay13, W. Geiss19, D. Gelé19,
C.E. Gerber51, Y. Gershtein49, D. Gillberg6, G. Ginther71, N. Golub41, B. Gómez8, A. Goussev82, P.D. Grannis72,
H. Greenlee50, Z.D. Greenwood60, E.M. Gregores4, G. Grenier29, Ph. Gris13, J.-F. Grivaiz16, A. Grohsjean25,
S. Grünendahl50, M.W. Grünendahl30, F. Guo72, J. Guo72, G. Gutierrez50, P. Gutierrez75, A. Haas70, N.J. Hadley61,
P. Haefner25, S. Hagopian49, J. Haley68, I. Hall65, R.E. Hall17, L. Han7, K. Harder44, A. Harel75, J.M. Hauptman57,
R. Hauen65, J. Hayes43, T. Hebbeker21, D. Hedin52, J.G. Hegeman34, A.P. Heinson48, U. Heintz62,
C. Hensen22d, K. Herner72, G. Hesketh63, M.D. Hildreth55, R. Hirosky81, J.D. Hobbs72, B. Hoeneisen12,
H. Hoeth26, M. Hohlfeld22, S.J. Hong53, S. Hosaini75, P. Houwen34, Y. Hu72, Z. Hubacek10, V. Hynek9,
I. Iashvili69, R. Illingworth50, A.S. Ito50, S. Jabben62, M. Jaffré16, S. Jain75, K. Jakobs23, C. Jarvis61, R. Jesik13,
K. Johns45, C. Johnson70, M. Johnson50, A. Jonckheere50, P. Jonsson43, A. Justo50, E. Kajfasz15, J.M. Kalk60,
D. Karmanov38, P.A. Kasper6, I. Katsanos70, D. Kau9, V. Kaushik78, R. Khec79, S. Kerniche15, N. Khalatyan50,
A. Khanov76, A. Kharchilava69, Y.M. Kharchev36, D. Khatsidze70, T.J. Kim31, M.H. Kirby53, M. Kirsch21,
B. Klima50, J.M. Kohli72, J.-P. Konrath53, A.V. Kozelov39, J. Kraus65, D. Krop54, T. Kuhl24, A. Kuma69,
A. Kupco11, T. Kurča20, V.A. Kuzmin38, J. Kvita9, F. Lacroix13, D. Lam55, S. Lammers70, G. Landsberg77,
P. Lebrun20, W.M. Lee50, A. Leflat38, J. Lellouch17, J. Leveque45, J.-J. Li78, L. Li48, Q.Z. Li50, S.M. Lietti5,
J.G.R. Lima52, D. Lincoln50, J. Linneweber50, V.V. Lipaev39, R. Lipton50, Y. Liu7, Z. Liu6, A. Lobodenko40,
M. Lokajicek11, P. Love42, H.J. Lubatti82, R. Luna4, A.L. Lyon50, A.K.A. Maciel2, D. Mackin80, R.J. Madaras46,
P. Mättig26, C. Martin21, A. Magerkurth64, P.K. Maiti82, H.B. Malbouisson3, S. Malik67, V.L. Malyshev36,
H.S. Mao50, Y. Maravin59, B. Martin14, R. McCarthy72, A. Mehnitchouk90, L. Mendoza8, P.G. Mercadante5,
M. Merkin48, K.W. Merritt50, A. Meyer21, J. Meyer22d, T. Millet20, J. Mitrevski70, R.K. Mommersen44,
N.K. Mondal29, R.W. Moore6, T. Moulik58, G.S. Muanza20, M. Mulhearn70, O. Mundal22, L. Mundim3,
E. Nagy13, M. Naimuddin68, M. Narain77, N.A. Naumann55, H.A. Neale64, P.J. Negret8, P. Neustroev40,
N. Nilsen23, H. Nobgina5, S.F. Novaes5, T. Nunnenmann39, V. O’Dell50, D.C. O’Neill5, G. Obrant50, C. Ochando16,
D. Onoprienko59, N. Oshima30, N. Osman43, J. Osta55, R. Oter10, G.J. Otero y Garzón50, M. Owen44, P. Padley80,
M. Pangilinan77, N. Parashar56, S.-J. Park22d, S.K. Park31, J. Parsons70, R. Partridge77, N. Parua54, A. Patwa73,
G. Pawloski80, B. Penning23, M. Perfiliev48, K. Peters44, Y. Peters26, P. Pétroff16, M. Petteni43, R. Piegaia1,
We present a measurement of the forward-backward charge asymmetry ($A_{FB}$) in $p\overline{p} \rightarrow Z/\gamma^* + X \rightarrow e^+e^- + X$ events at a center-of-mass energy of 1.96 TeV using 1.1 fb$^{-1}$ of data collected with the D0 detector at the Fermilab Tevatron collider. $A_{FB}$ is measured as a function of the invariant mass of the electron-positron pair, and found to be consistent with the standard model prediction. We use the $A_{FB}$ measurement to extract the effective weak mixing angle $\sin^2 \theta_{\text{eff}}^W = 0.2326 \pm 0.0018$ (stat.) $\pm 0.0006$ (syst.).

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In the standard model (SM), the neutral-current couplings of the Z bosons to fermions (f) at tree level are defined as

\[ -i \frac{g}{2 \cos \theta_W} \cdot \vec{f} \gamma^\mu (g_V^f - g_A^f \gamma_5) f \cdot Z^\mu \]  

(1)

where \( \theta_W \) is the weak mixing angle, and \( g_V^f \) and \( g_A^f \) are the vector and axial-vector couplings with \( g_V^f = I_3^f - 2Q_f \sin^2 \theta_W \) and \( g_A^f = I_3^f \). Here \( I_3^f \) is the weak isospin component of the fermion and \( Q_f \) its charge. The presence of both vector and axial-vector couplings in \( qq \rightarrow Z/\gamma^* \rightarrow \ell^+\ell^- \) gives rise to an asymmetry in the polar angle (\( \theta \)) of the negatively charged lepton momentum relative to the incoming quark momentum in the rest frame of the lepton pair. The angular differential cross section can be written as

\[ \frac{d\sigma}{d\cos \theta} = A(1 + \cos^2 \theta) + B \cos \theta, \]  

(2)

where \( A \) and \( B \) are functions dependent on \( I_3^f \), \( Q_f \), and \( \sin^2 \theta_W \). Events with \( \cos \theta > 0 \) are called forward events, and those with \( \cos \theta < 0 \) are called backward events.

The forward-backward charge asymmetry, \( A_{FB} \), is defined as

\[ A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B}, \]  

(3)

where \( \sigma_{F/B} \) is the integral cross section in the forward/backward configuration. We measure \( A_{FB} \) as a function of the invariant mass of the lepton pair. To minimize the effect of the unknown transverse momenta of the incoming quarks in the measurement of the forward and backward cross sections, we use \( \theta \) calculated in the Collins-Soper reference frame \( \Gamma \). In this frame, the polar axis is defined as the bisector of the proton beam momentum and the negative of the anti-proton beam momentum when they are boosted into the rest frame of the lepton pair.

The forward-backward asymmetry is sensitive to \( \sin^2 \theta_W^{\text{eff}} \), which is an effective parameter that includes higher order corrections. The current world average value of \( \sin^2 \theta_W^{\text{eff}} \) at the Z-pole is 0.23149 ± 0.00013 \( [2] \). Two \( \sin^2 \theta_W^{\text{eff}} \) measurements are more than two standard deviations from the world average value: that from the charge asymmetry for b quark production (\( A_{FB}^{bb} \)) from the LEP and SLD collaborations \( [3] \) and that from neutrino and antineutrino cross sections from the NuTeV collaboration \( [4] \). The \( A_{FB}^{bb} \) measurement is sensitive to the couplings of b quarks to the Z boson, and the NuTeV measurement is sensitive to the couplings of u and d quarks to the Z boson, as is the measurement presented here. Previous direct measurements of u and d quark couplings to the Z are of limited precision \( [5, 6] \). Thus, modifications to the SM that would affect only u and d couplings are poorly constrained. In addition, \( A_{FB} \) measurements at the Tevatron can be performed up to values of the dilepton mass exceeding those achieved at LEP and SLC, therefore becoming sensitive to possible new physics effects \( [7, 8] \). Although direct searches for these new phenomena in the \( Z/\gamma^* \rightarrow \ell^+\ell^- \) final state have been recently performed by the CDF and D0 collaborations \( [9] \), charge asymmetry measurements are sensitive to different combination of couplings, and can provide complementary information \( [10] \).

The CDF collaboration measured \( A_{FB} \) using 108 pb\(^{-1} \) of data in Run I \( [11] \) and 72 pb\(^{-1} \) of data in Run II \( [3] \). This analysis uses 1066 ± 65 pb\(^{-1} \) of data collected with the D0 detector \( [12] \) at the Fermilab Tevatron collider at a center-of-mass energy of 1.96 TeV to measure the \( A_{FB} \) distribution and extract \( \sin^2 \theta_W^{\text{eff}} \).

To select \( Z/\gamma^* \) events, we require two isolated electromagnetic (EM) clusters that have shower shapes consistent with that of an electron. EM candidates are required to have transverse momentum \( p_T > 25 \) GeV. The dielectron pair must have a reconstructed invariant mass \( 50 < M_{ee} < 500 \) GeV. If an event has both its EM candidates in the central calorimeter (CC events), each must be spatially matched to a reconstructed track in the tracking system. Because the tracking efficiency decreases with magnitude of the rapidity in the end calorimeter, events with one candidate in the central and one candidate in the end calorimeter (CE events) are required to have a matching track only for that in the central calorimeter. For CC events, the two candidates are further required to have opposite charges. For CE events, the determination of forward or backward is made according to the charge of the EM candidate in the central calorimeter. A total of 35,626 events remain after application of all selection criteria, with 16,736 CC events and 18,890 CE events. The selection efficiencies are measured using \( Z/\gamma^* \rightarrow ee \) data with the tag-probe method \( [14] \), and no differences between forward and backward events are observed.

The asymmetry is measured in 14 \( M_{ee} \) bins within the \( 50 < M_{ee} < 500 \) GeV range. The bin widths are determined by the mass resolution, of order \((3 - 4)\%\), and event statistics.

Monte Carlo (MC) samples for the \( Z/\gamma^* \rightarrow e^+e^- \) process are generated using the \textsc{pythia} event generator \( [15] \) using the CTEQ6L1 parton distribution functions (PDFs) \( [16] \), followed by a detailed \textsc{geant}-based simulation of the D0 detector \( [17] \). To improve the agreement between data and simulation, selection efficiencies determined by the MC are corrected to corresponding values measured in the data. Furthermore, the simulation is tuned to reproduce the calorimeter energy scale and resolution, as well as the distributions of the instantaneous luminosity and z position of the event primary vertex observed in data. Next-to-leading order (NLO) quantum chromodynamics (QCD) corrections for \( Z/\gamma^* \) boson production \( [18, 19] \) are applied by reweighting the \( Z/\gamma^* \) boson transverse momentum, rapidity, and invariant mass.
distributions from PYTHIA.

The largest background arises from photon+jets and multijet final states in which photons or jets are misreconstructed as electrons. Smaller background contributions arise from electroweak processes that produce two real electrons in the final state. The multijet background is estimated using collider data by fitting the electron isolation distribution in data to the sum of the isolation distributions from a pure electron sample and an EM-like jet sample. The pure electron sample is obtained by enforcing tighter track matching requirements on the two electrons with $80 < M_{ee} < 100$ GeV. The EM-like jets sample is obtained from a sample where only one good EM cluster and one jet are back-to-back in azimuthal angle $\phi$. The contamination in the EM-like jets sample from $W \to e\nu$ events is removed by requiring missing transverse energy $E_T < 10$ GeV. The average multijet background fraction over the entire mass region is found to be approximately 0.9%. Other SM backgrounds due to $W + \gamma$, $W+$jets, $WW$, $WZ$, and $t\bar{t}$ are estimated separately for forward and backward events using PYTHIA events passed through the GEANT simulation. Higher order corrections to the PYTHIA leading order (LO) cross sections have been applied [19, 20, 21]. These SM backgrounds are found to be negligible for almost all mass bins. The $Z/\gamma^* \to \tau^+\tau^-$ contribution is similarly negligible.

In the SM, the $A_{FB}$ distribution is fully determined by the value of $\sin^2 \theta^W_{eff}$ in a LO prediction for the process $q\bar{q} \to Z/\gamma^* \to e^+e^-$. The value of $\sin^2 \theta^W_{eff}$ is extracted from the data by comparing the background-subtracted raw $A_{FB}$ distribution with templates corresponding to different input values of $\sin^2 \theta^W_{eff}$ generated with PYTHIA and GEANT-based MC simulation. Although $\sin^2 \theta^W_{eff}$ varies over the full mass range $50 < M_{ee} < 500$ GeV, it is nearly constant over the range $70 < M_{ee} < 130$ GeV. Over this region, we measure $\sin^2 \theta^W_{eff} = 0.2321 \pm 0.0018$ (stat.) $\pm 0.0006$ (syst.). The primary systematic uncertainties are due to the PDFs (0.0005) and the EM energy scale and resolution (0.0003). We include higher order QCD and electroweak corrections using the ZGRAD2 [22] program with the generator-level $Z/\gamma^*$ boson $p_T$ distribution tuned to match our measured distribution [23]. The effect of higher order corrections results in a central value of $\sin^2 \theta^W_{eff} = 0.2326$ [24].

Due to the detector resolution, events may be reconstructed in a different mass bin than the one in which they were generated. The CC and CE raw $A_{FB}$ distributions are unfolded separately and then combined. The unfolding procedure is based on an iterative application of the method of matrix inversion [25]. A response matrix is computed as $R^{BB}_{ij}$ for an event that is measured as forward in $M_{ee}$ bin $i$ to be found as forward and in bin $j$ at the generator level. Likewise, we also calculate the response matrices for backward events being found as backward ($R^{BB}_{ij}$), forward as backward ($R^{FB}_{ij}$), and backward as forward ($R^{BF}_{ij}$). Four matrices are calculated from the GEANT MC simulation and used to unfold the raw $A_{FB}$ distribution. The method was verified by comparing the true and unfolded spectrum generated using pseudo-experiments.

The data are further corrected for acceptance and selection efficiency using the GEANT simulation. The overall acceptance times efficiency rises from 3.5% for $50 < M_{ee} < 60$ GeV to 21% for $250 < M_{ee} < 500$ GeV.

The electron charge measurement in the central calorimeter determines whether an event is forward or backward. Any mismeasurement of the charge of the electron results in a dilution of $A_{FB}$. The charge misidentification rate, $f_Q$, is measured using GEANT-simulated $Z/\gamma^* \to e^+e^-$ events tuned to the average rate measured in data. The misidentification rate rises from 0.21% at $50 < M_{ee} < 60$ GeV to 0.92% at $250 < M_{ee} < 500$ GeV. The charge misidentification rate is included as a dilution factor $D$ in $A_{FB}$, with $D = (1 - f_Q)/(1 - f_Q + f_Q^2)$ for CC events and $D = (1 - f_Q)$ for CE events.

The final unfolded $A_{FB}$ distribution using both CC and CE events is shown in Fig. 1 compared to the PYTHIA prediction using the CTEQ6L1 PDFs [16] and the ZGRAD2 prediction using the CTEQ5L PDFs [26]. The $\chi^2$/d.o.f. with respect to the PYTHIA prediction is 16.1/14 for CC, 8.5/14 for CE, and 10.6/14 for CE and CE combined. The systematic uncertainties for the unfolded $A_{FB}$ distribution arise from the electron energy scale and resolution, backgrounds, limited MC samples used to calculate the response matrices, acceptance and efficiency corrections, charge misidentification and PDFs. The unfolded $A_{FB}$ together with the PYTHIA and ZGRAD2 predictions for each mass bin can be found in Table 1. The correlations between invariant mass bins are shown in Table II.

In conclusion, we have measured the forward-backward charge asymmetry for the $p\bar{p} \to Z/\gamma^* + X \to e^+e^- + X$ process in the dilepton invariant mass range $50 - 500$ GeV using $1.1$ fb$^{-1}$ of data collected by the D0 experiment. The measured $A_{FB}$ values are in good agreement with the SM predictions. We use the $A_{FB}$ measurements in the range $70 < M_{ee} < 130$ GeV to determine $\sin^2 \theta^W_{eff} = 0.2326 \pm 0.0018$ (stat.) $\pm 0.0006$ (syst.). The precision of this measurement is comparable to that obtained from LEP measurements of the inclusive hadronic charge asymmetry [3] and that of NuTeV measurement [4]. Our measurements of $\sin^2 \theta^W_{eff}$ in a dilepton mass region dominated by $Z$ exchange, which is primarily sensitive to the vector coupling of the $Z$ to the electron, and of $A_{FB}$ over a wider mass region, which is in addition sensitive to the couplings of the $Z$ to light quarks, agree well with predictions. With about 8 fb$^{-1}$ of data expected by the end of Run II, a combined measurement of $A_{FB}$ by the CDF and D0 collaborations using electron and muon final states could lead to a measurement of $\sin^2 \theta^W_{eff}$ with a precision comparable to that of the current.
world average. Further improvements to current MC generators, incorporating higher order QCD and electroweak corrections, would enable the use of such measurement in a global electroweak fit.

![Graph](image)

**FIG. 1:** Comparison between the unfolded $A_{FB}$ (points) and the **pythia** (solid curve) and **zgrad2** (dashed line) predictions. The inner (outer) vertical lines show the statistical (total) uncertainty.

| $M_{ee}$ range (GeV) | Predicted $A_{FB}$ | Unfolded $A_{FB}$ |
|------------------|------------------|------------------|
| (GeV) | (GeV) | **pythia** | **zgrad2** | |
| 50 – 60 | 64.5 | $-0.233$ | $-0.307$ | $-0.362 \pm 0.066 \pm 0.072$ |
| 60 – 70 | 64.9 | $-0.426$ | $-0.431$ | $-0.434 \pm 0.039 \pm 0.040$ |
| 70 – 75 | 72.6 | $-0.449$ | $-0.452$ | $-0.386 \pm 0.032 \pm 0.031$ |
| 75 – 80 | 78.3 | $-0.354$ | $-0.354$ | $-0.342 \pm 0.022 \pm 0.022$ |
| 81 – 86.5 | 84.4 | $-0.174$ | $-0.166$ | $-0.176 \pm 0.012 \pm 0.014$ |
| 86.5 – 90.5 | 88.4 | $-0.033$ | $-0.031$ | $-0.034 \pm 0.007 \pm 0.008$ |
| 90.5 – 92 | 90.9 | 0.051 | 0.052 | $0.048 \pm 0.006 \pm 0.005$ |
| 92 – 97 | 93.4 | 0.127 | 0.129 | $0.122 \pm 0.006 \pm 0.007$ |
| 97 – 105 | 99.9 | 0.289 | 0.296 | $0.301 \pm 0.013 \pm 0.015$ |
| 105 – 115 | 109.1 | 0.427 | 0.429 | $0.416 \pm 0.030 \pm 0.022$ |
| 115 – 130 | 121.3 | 0.526 | 0.530 | $0.543 \pm 0.039 \pm 0.028$ |
| 130 – 180 | 147.9 | 0.593 | 0.603 | $0.617 \pm 0.046 \pm 0.013$ |
| 180 – 250 | 206.4 | 0.613 | 0.606 | $0.594 \pm 0.085 \pm 0.016$ |
| 250 – 500 | 310.5 | 0.616 | 0.615 | $0.320 \pm 0.150 \pm 0.018$ |

**TABLE I:** The first column shows the mass ranges used. The second column shows the cross section weighted average of the invariant mass in each mass bin derived from **pythia**. The third and fourth columns show the $A_{FB}$ predictions from **pythia** and **zgrad2**. The last column is the unfolded $A_{FB}$: the first uncertainty is statistical, and the second is systematic.

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| Mass bin | 1   | 2   | 3   | 4   | 5   | 6   | 7   | 8   | 9   | 10  | 11  | 12  | 13  | 14  |
|---------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 1       | 1.00| 0.21| 0.04| 0.00| 0.00| 0.01| 0.00| 0.01| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00|
| 2       | 1.00| 0.42| 0.08| 0.02| 0.01| 0.02| 0.01| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00|
| 3       | 1.00| 0.49| 0.13| 0.04| 0.03| 0.02| 0.01| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00|
| 4       | 1.00| 0.52| 0.16| 0.08| 0.04| 0.01| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00|
| 5       | 1.00| 0.72| 0.32| 0.11| 0.01| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00|
| 6       | 1.00| 0.80| 0.15| 0.01| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00|
| 7       | 1.00| 0.50| 0.04| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00|
| 8       | 1.00| 0.38| 0.04| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00|
| 9       | 1.00| 0.30| 0.01| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00|
| 10      | 1.00| 0.14| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00|
| 11      | 1.00| 0.06| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00|
| 12      | 1.00| 0.06| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00|
| 13      | 1.00| 0.06| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00|
| 14      | 1.00| 0.06| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00| 0.00|

TABLE II: Correlation coefficients between different $M_{ee}$ mass bins. Only half of the symmetric correlation matrix is presented.

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