Temperature induced crossing in the optical bandgap of mono and bilayer MoS$_2$ on SiO$_2$

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Photoluminescence measurements in mono- and bilayer-MoS$_2$ on SiO$_2$ were undertaken to determine the thermal effect of the MoS$_2$/SiO$_2$ interface on the optical bandgap. The energy and intensity of the photoluminescence from monolayer MoS$_2$ were lower and weaker than those from bilayer MoS$_2$ at low temperatures, whilst the opposite was true at high temperatures above 200 K. Density functional theory calculations suggest that the observed optical bandgap crossover is caused by a weaker substrate coupling to the bilayer than to the monolayer.

The discovery of unique transport properties of graphene prepared by mechanical exfoliation has spurred many new research activities for future electronic devices because of graphene's intriguing energy band structure and high carrier mobility$^{1-3}$. Although graphene is a promising material due to its rich physics, pristine graphene has no bandgap which can limit application areas. As alternatives, layered two-dimensional (2D) materials composed of transition metal dichalcogenides (TMDs) such as MX$_2$ ($M$ = Mo, W, and X = S, Se) have been the centre of attention for applications in next-generation nanoelectronic and optoelectronic devices because of their unusual valley and optical polarization properties. Amongst them, MoS$_2$ can provide both indirect and direct bandgap transitions depending on the layer thickness$^{4-6}$. A monolayer (1L) of MoS$_2$ (1L-MoS$_2$) is a direct gap semiconductor with a band gap of 1.8~1.9 eV at the K-points of the 2D hexagonal Brillouin zone, whereas bulk MoS$_2$ is an indirect semiconductor with a band gap of $\sim$1.2 eV$^{4-6}$. These findings have boosted the development of 2D materials for high-performance flexible electronic and optoelectronic devices$^{7,8}$. There has been much interest generated in studying the characteristic optical properties of MoS$_2$ using photoluminescence (PL) measurements as well as the valleytronics related to its 2D symmetry$^{9-15}$. However, the electrical and optical properties of the MoS$_2$ can be greatly affected by its surface and also by the MoS$_2$/substrate interface. It is therefore important to understand how such interfaces can affect the optical and electronic features of the material. Moreover, the PL intensity depends on the number of layers, indicating that the quantum efficiency can decrease with layer thickness and whether the flake is freestanding or on a substrate$^6$. Note that when MoS$_2$ layers lie on a substrate, each layer undergoes a different strain between the substrate and the MoS$_2$ layers because the first layer of MoS$_2$ is in direct contact with the substrate, whilst the other layers interact weakly due to van der Waals bonding between the MoS$_2$ layers, which can affect the optical transition between the 1L-MoS$_2$ and the other layers.

In this letter, we demonstrate temperature dependent PL behaviour of mechanically-exfoliated 1L- and bilayer (2L) MoS$_2$ prepared on a SiO$_2$ substrate. The PL peak's intensity and energy for the 2L-MoS$_2$ are stronger and higher than those of the 1L-MoS$_2$ at low temperatures below 200 K, in contrast to the room temperature measurements, where the opposite occurs. In order to explain this phenomenon, density functional theory (DFT) calculations are performed taking into account the thermal expansion at the MoS$_2$/SiO$_2$ interface.

Results

Figure 1(b,c) show the PL spectral maps measured at the 1L- and 2L-MoS$_2$ flake which are consistent with the optical microscopy image in Fig. 1(a). Figure 1(d~g) show the PL spectra of the 1L- and 2L-MoS$_2$ flakes, extracted from the circle points of the maps measured at 4.2 K, 100 K, 200 K and 292 K, respectively. The PL intensity

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measured at 4.2 K is similar across both the 1L- and 2L-MoS 2 regions. However, by inspecting the PL spectra taken at 4.2 K along the dotted line on the 1L- and 2L-MoS 2 as shown in Fig. 1(d), the intensity of the 2L-MoS 2 is slightly more intense than that of 1L-MoS 2. In addition, a prominent PL peak can be identified at a higher energy of ~1.869 eV for 1L-MoS 2 than 1.876 eV for 2L-MoS 2 at 4.2 K, while the opposite is true at room temperature as shown in Fig. 1(g). We have checked the variation of PL intensity and emission energy for the 1L- and 2L-MoS 2 at the several temperatures. The PL peak's intensity and energy for the 2L-MoS 2 are more intense and higher than those of the 1L-MoS 2 up to 150 K, whilst the energies are almost the same near 200 K (Fig. 2(f)) and then become inverted at room temperature, which is consistent with previous reports 6. The boundary between the 1L- and 2L-MoS 2 regions indicated in the optical microscope image can be seen clearly. The abrupt PL intensity difference between 1L- and 2L-MoS 2 at 292 K coincides with the corresponding regions of the optical microscopy image, confirming the difference in PL collected from the two distinct areas of the flake. The observed room-temperature PL behavior of the 1L- and 2L-MoS 2 is in contrast to the previous reports, stating that the PL intensity of the MoS 2 decreases with increasing layer thickness 6. We should consider the relationship of the emission energy and the physical nature of the MoS 2/SiO 2 interface, which may cause different strain in 1L- and 2L-MoS 2. Mechanical strain can reduce the optical band gap by ~45 meV/% for monolayer MoS 2 and ~120 meV/% for bilayer MoS 2 16, where the role of substrate is unclear. Similar PL characteristics were observed in another flake on the same SiO 2 substrate, confirming that this phenomenon is reproducible (Fig. S1) 17.
The detailed PL intensity variations across the flake (dotted lines of Fig. 1(b,c)) are presented in Fig. 2. The PL intensity and energy at 4.2 K becomes slightly weaker and redshifts across the 2L-MoS$_2$ to 1L-MoS$_2$ boundaries as shown in Fig. 2(b). However, the opposite behavior is seen above 200 K, and the signal becomes more intense with increasing $x$ position, as shown in Fig. 2(a).

Figure 3 shows the PL peak energies for the 1L and 2L-MoS$_2$ and their intensity ratio (I$_{1L}$/I$_{2L}$) as a function of temperature. The PL peaks shift to lower energy with increasing temperature. The temperature-dependent optical bandgap variation is understood in terms of lattice dilation and electron-lattice interactions. We can clearly see that the peak energy crosses over around 200 K. In addition, the intensity of the 1L-MoS$_2$ becomes more intense in the high temperature region above ~200 K. The temperature dependence of the bandgap proposed by O’Donnell and Chen takes into account the influence of phonons on the bandgap energy to obtain a better fit for semiconductors at lower temperatures$^{18}$. They considered the following equation:

$$E_g(T) = E_g(0) - S \left( \frac{\langle E_{ph} \rangle}{2kT} \coth \left( \frac{\langle E_{ph} \rangle}{2kT} \right) - 1 \right),$$

where $\langle E_{ph} \rangle$ is an average phonon energy and $S$ is a dimensionless coupling constant. The measured data are in good agreement with the aforementioned relationship at all measured temperatures (black solid line for 1L-MoS$_2$ and blue solid line for 2L-MoS$_2$). The extracted $\langle E_{ph} \rangle$ value is ~37.8 meV for the 1L-MoS$_2$ and 33.1 meV for the 2L-MoS$_2$. The theoretical LO inter-valley phonon energy of the 1L-MoS$_2$ is 41 meV$^{19}$, which is close to our fitted value. The green line is the fitting curve for the 1L-MoS$_2$ with $\langle E_{ph} \rangle = 41$ meV.

Discussion

In order to explain the observed crossing behavior of the optical bandgap of the 1L- and 2L-MoS$_2$ with increasing temperature, DFT calculations were carried out focusing on the effect of the substrate. The effect of electron-phonon coupling on the energy gap can be recast in terms of the lattice thermal expansion as an equivalent phenomenological description$^{18}$. Furthermore, the interface electronic coupling should be nearly independent of temperature, because the band edge states at the K or K' valley mainly arise from Mo d orbitals with a negligible coupling to the O or Si atomic orbitals of the substrate. The band alignment is type I with a much wider energy gap for SiO$_2$ than MoS$_2$.$^{20,21}$ Thus, the temperature dependence of the energy gap can be understood by

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**Figure 2.** $\mu$-PL spectra maps at 292 K (a) and 4.2 K (b), measured along the dotted lines in the intensity maps of Fig. 1(b,c). The red arrows are the guide for eyes indicating the PL peak's energy and intensity variation from 2L- to 1L-MoS$_2$.

**Figure 3.** PL energy and integrated PL intensity ratio of the 1L- and 2L-MoS$_2$ as a function of temperature. The solid lines are fitting curves using the O’Donnell and Chen equation.
the thermal expansion of the 1L- or 2L-MoS₂ themselves. For example, the lowest MoS₂ layer will have a different coupling strength to the underlying substrate for 1L-MoS₂ due to an additional van der Waals attraction in bilayer MoS₂, thus the in-plane thermal expansion can be different for 1L- and 2L-MoS₂.

The relative coupling strength is studied by calculating the binding energy between 1L-MoS₂ and SiO₂, and comparing that to the interlayer binding energy of 2L-MoS₂, where the Perdew-Burke-Ernzerhof (PBE) type generalized gradient approximation is used together with the D2 method for the van der Waals (vdW) correction. The binding energy between 1L-MoS₂ and SiO₂ is calculated by \( E_{b}^{1L-MoS_2/SiO_2} = E_{1L-MoS_2,SiO_2} - E_{1L-MoS_2} - E_{SiO_2} \), where \( E_{1L-MoS_2,SiO_2} \) is the total energy of the adsorbed system, \( E_{1L-MoS_2} \) and \( E_{SiO_2} \) are the energies of 1L-MoS₂ and SiO₂, respectively, for its own optimized lattice constant. The calculated binding energy is \(-139\) meV per MoS₂ unit, in good agreement with theoretical reports, indicating that adsorption of 1L-MoS₂ on SiO₂ is energetically favorable. However, the interlayer binding energy of 2L-MoS₂ is calculated to be \(-146\) meV per MoS₂ unit, which is \(7\) meV/MoS₂ more stable than the adsorption of the monolayer. We note that using the Tkatchenko and Scheffler type vdW correction gives qualitatively the same result (304 meV for MoS₂-MoS₂ versus 235 meV MoS₂-SiO₂). Thus, the bottom MoS₂ layer in 2L-MoS₂ should be less coupled to the SiO₂ than the upper layer, giving rise to almost free-standing 2L-MoS₂.

The average phonon energy \( <E_{ph}> \) extracted from the fitting in Fig. 3 is closer to the energy of the in-plane phonon mode (\( E_{g} \)) than that of the out-of-plane mode (\( A_{1g} \)), which means that the in-plane thermal expansion can be used to understand the observed PL gap behavior. Since the 1L-MoS₂ has a stronger coupling to the SiO₂ substrate than 2L-MoS₂ according our theoretical calculation, the in plane thermal expansion of 1L-MoS₂ should be suppressed compared to that of 2L-MoS₂, due to a larger contribution from the lighter elements (Si and O) in the vibration, where the thermal expansion coefficient (TEC) of SiO₂ is \(-10^{-6}/K\), and the in-plane TEC of bulk MoS₂ was measured to be \(-5.0 \times 10^{-5}/K\), and a monolayer of MoS₂ has a much larger value \(-24.4 \times 10^{-6}/K\) from a recent measurement. Thus, a smaller expansion of 1L-MoS₂ than 2L-MoS₂ arises when the thermal expansion is modified by the substrate coupling. Then as the lattice parameters increase, the direct energy gap variation can be used to explain the observed temperature dependence of the gap, as long as the substrate electronic coupling is independent of temperature and the phenomenological description of ref. 18 for the electron-phonon coupling via lattice thermal expansion holds true for our system.

Figure 4(a) shows the direct gaps calculated for free-standing 1L- and 2L-MoS₂ indicated by the filled squares and circles, respectively, where the PBE type functional used is sufficient for qualitative analysis. We have chosen certain lattice constants larger than the experimental value \( a_{exp} = 3.16 \) Å. Each of 1L- and 2L-MoS₂ exhibits a linear variation with an almost equal slope (\(-3.0\) eV/Å), where only three data points are displayed in Fig. 4(a) among ten points from 0.0 to 0.16 Å expansion relative to \( a_{exp} \). By using the reported TEC \(-2 \times 10^{-5}/K\), we obtain \(-0.02\) Å lattice expansion with a temperature increase of 300 K, thereby predict 60 meV decrease in the gap, as illustrated by the blue dashed arrow in Fig. 4(a). Assuming a full strain of 2L-MoS₂, it matches well to our experimental result. To explain the crossover behavior, however, we have to choose a suitable size of the gap for 1L-MoS₂ at low temperature, which is smaller than that of 2L-MoS₂ as observed in the experiment. Actually, our calculated energy gap with including the spin orbit coupling shows larger gap for 2L-MoS₂ than 1L-MoS₂, as shown in Fig. 4(b). With a smaller expansion for 1L-MoS₂, (black dashed arrow in Fig. 4(a) corresponds to half of that for 2L-MoS₂), a crossing behavior of the 1L- and 2L-MoS₂ energy gaps upon thermal expansion can be obtained. Also Fig. 4(b) shows that the intensity is larger for 2L-MoS₂ than 1L-MoS₂, which matches with the low temperature observation. This is because the degeneracy is doubled in 2L-MoS₂ by the presence of the inversion
symmetry. The crossing behavior of PL intensity with increasing temperature can be described qualitatively by the enhanced phonon coupling towards the indirect emission in the indirect gap 2L-MoS₂, thereby the original direct emission will be suppressed in 2L-MoS₂ whilst it is essentially unaffected in the direct gap 1L-MoS₂.

In summary, we have demonstrated an abnormal behaviour in the excitonic photoluminescence of 1L- and 2L-MoS₂. The PL peak's energy and intensity of monolayer MoS₂ are lower and weaker compared to bilayer MoS₂ at low temperatures, whilst the opposite is true at high temperatures above 200 K. The DFT calculations suggest that the observed crossing of the optical bandgap with increasing temperature is due to different thermal expansion coefficients of the 1L- and 2L-MoS₂ at the MoS₂/SiO₂ interface, causing weaker substrate coupling to the bilayer than to the monolayer, which enhances the redshift of the bilayer MoS₂.

**Methods**

**Preparation and characterization of 1L- and 2L-MoS₂.** The 1L- and 2L-MoS₂ flakes were prepared on a SiO₂/Si substrate by mechanical exfoliation from natural MoS₂ as shown in Fig. 1(a) and the number of MoS₂ layers was characterized by micro-Raman spectroscopy that the frequency differences between the in-plane (E₁g) and out-of-plane (A₁g) modes are 17.77 cm⁻¹ for the 1L-MoS and 20.01 cm⁻¹ for the 2L-MoS₂ (Fig. S2), which are in good agreement with values in the literature⁵⁸. For the low temperature PL measurements, the sample was mounted in a continuous-flow helium cryostat, allowing the temperature to be controlled accurately from low temperature (4.2 K) to room temperature and the optical luminescence properties were characterized by using micro-photoluminescence (µ-PL). A CW linearly polarized solid-state laser operating at a wavelength of 532 nm was used for the excitation of the MoS₂ flake. A 100 × (NA 0.7) objective was held above the cryostat focusing the incident laser beam to a spot size of ~0.8 μm² and also to collect the emitted luminescence from the same spot.

**Calculations**

The atomic structure is modelled as a slab, which includes six atomic layers and 20 Å vacuum space, and bottom Si dangling bonds are passivated by H (Fig. S3). It should be noted that the substrate involves O dangling bonds and 4.90 Å (experimental value is 4.91 Å), respectively. The optimized vertical distance between the lowest S and lattice constants for pristine MoS₂ and SiO₂ are in good agreement with values in the literature²⁸. For the low temperature PL measurements, the sample was matching 3

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Acknowledgements
This research was supported by Basic Science Research Program through the National Research Foundation of Korea (NRF) funded by the Ministry of Education, Science and Technology (Grant No. 2015R1D1A1A01058332, 2015R1C1A1A01055922, 2016R1D1A1B03935688, 2015M2A2A6A02045252, 2015R1A2A2A01004782 and 2016R1A6A1A03012877).

Author Contributions
Y.P., R.A.T., H.I. and G.L. designed this work and prepared the manuscript. The experimental and optical measurements were performed by Y.P., C.C.S.C. and Y.J., Y.K. and G.L. carried out DFT calculations. S.W.L. and W.Y. and N.K. discussed the manuscript during the preparation. All authors discussed the results and implications and commented on the manuscript at all stage.

Additional Information
Supplementary information accompanies this paper at https://doi.org/10.1038/s41598-018-23788-3.

Competing Interests: The authors declare no competing interests.

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