Charged Particle Multiplicities in A+A and p+p Collisions in the Constituent Quarks Framework

Rachid Nouicer
Brookhaven National Laboratory, Upton, New York 11973-5000, U.S.A.

Received: date / Revised version: date

Abstract. Charged particle multiplicities in A+A and p(\bar{p}) + p collisions as a function of pseudorapidity, centrality and energy are studied in both the nucleon and the constituent quark frameworks. In the present work, the calculation of the number of nucleon and constituent quark participants using the nuclear overlap model takes into account the fact that for the peripheral A+A and p+p collisions can not be smaller than two. A striking agreement is seen between the particle density in A+A and p(\bar{p}) + p collisions, both at mid-rapidity and in the fragmentation regions, when normalized to the number of participating constituent quarks. The observations presented in this paper imply that the number of constituent quark pairs participating in the collision controls the particle production. One may therefore conjecture that the initial states in A+A and p(\bar{p}) + p collisions are similar when the partonic considerations are used in normalization.

PACS. 25.75.-q, 25.75.Dw, 25.75.Nq, 24.10.Jv

1 -Introduction

Quantum Chromo-Dynamics (QCD) is the theory of strong interactions. From a theorist’s point of view strong interaction means that all dimensionless quantities of the theory are of the order of unity. Meanwhile, there are at least two fundamental facts about strong interactions showing that actually it is not exactly so: there are still certain small parameters hidden. One is that nuclei can be viewed as made of weakly bound nucleons – in a true strong interactions case they would rather look like a quark soup. The second puzzle is that the nucleon itself can be viewed as built of three constituent quarks (objects quasi-free non relativistic) – in a true strong interactions case it would rather look like a pack of an indefinite number of quarks, antiquarks and gluons. The presence of just three discrete objects in a nucleon is non-trivial from the point of view of the parton model, which permits any large number of point-like objects, i.e. quark-partons, inside a fast moving nucleon. The two notions can be reconciled if one accepts a nucleon with two radii: a nucleon radius \( R_n \) that determines a mean distance between the constituent quarks, and a proper radius of the constituent, \( r_q \). In such a pattern, a fast moving nucleon is a viewed as a system of three clouds of partons, each containing a valence quark, a sea of the quark-antiquark pairs, and gluons. QCD calculations support the statement that inside a nucleon there are three objects of size of 0.1-0.3 fm [1]. Similar idea is applied in the study of multihadron production processes in different types of collisions in the framework of the picture based on dissipating energy of participants [2].

In this paper, I illustrate a modified version on how to calculate the number of nucleon and constituent quark participants. One problem in previous calculations [3, 4] was confusion in applying the appropriate minimum-bias \( \langle N_{part}^n \rangle \) to the p(\bar{p}) + p collisions. A second, more general problem in the previous calculation which can be found in the Refs. 3,4,5 stems from the fact that in the nuclear overlap model in peripheral collisions the number of nucleon and constituent quark participants (\( \langle N_{part}^n \rangle \) and \( \langle N_{part}^q \rangle \)) can be smaller than two – this is because, in peripheral limit, the overlap integral has a meaning of 1/2 times the probability to have \( \langle N_{part}^n \rangle =2 \). In the previous calculation [3,4,5], the problem can be found in the estimate of \( \langle N_{part}^n \rangle \) for the peripheral A+A collisions and easily from the calculation of the number of constituent quark participants for p+p collisions such plotting \( \langle N_{part}^q \rangle \) versus collision centrality or impact parameter. A similar problem with the calculation of \( \langle N_{part}^n \rangle \) for d+Au collisions using an optical approach has been reported by D. Kharzeev et al. [6]. The goal of the present paper is to study the charged particle multiplicities in the nucleus-nucleus (A+A) and nucleon-nucleon (p(\bar{p}) + p) collisions in both the nucleon and the constituent quark frameworks.

The motivations of this study are: nuclear collisions are studied at unprecedented energies at the Relativistic Heavy Ion Collider (RHIC), revealing several new phenomena embedded in a large amount of high-quality data [7]. However, several aspects of the results on charged par-
particle multiplicities in the nucleon framework (results scaled to the number of nucleon participants) are still not well understood such as:

1. the charged particle densities near mid-rapidity region in Au+Au at 200 GeV depend strongly on the collision centrality. The densities have been plotted as per nucleon participants pair \[3\] in order to disentangle pure nuclear effects. The common explanation of the phenomena is due to the hard processes.

2. the charged particle density at mid-rapidity region from A+A collisions are substantially higher than those of p(\bar{p}) + p collisions at the same energy \[4, 5\].

3. the charged particle densities at the fragmentation region from A+A collisions are substantially higher than those of p(\bar{p}) + p collisions at the same energy \[4\].

4. the integrated total charged particle in A+A collisions as a function of number nucleon participants is higher than p(\bar{p}) + p collisions at the same energy indicating that there is no smooth transition between A+A and nucleon-nucleon collisions \[11\].

The investigations on the aspects 1. and 2. have been already started in Refs. \[3, 4, 5\] using the old version which contains problem in the calculations of \(\langle N^p_{\text{part}} \rangle\) and \(\langle N^q_{\text{part}} \rangle\) for peripheral A+A collisions and p(\bar{p}) + p collisions. In this paper, I will review the aspects 1. and 2. and I will extend the investigation to study the aspects 3. and 4. in both the nucleon and constituent quark frameworks, using the new version of the calculation.

2 - Calculation of the Number of Participants

The number of nucleon participants noted by \(\langle N^p_{\text{part}} \rangle\), and the number of constituent quark participants noted by \(\langle N^q_{\text{part}} \rangle\), are estimated using the nuclear overlap model in a manner similar to that used in Refs. \[3, 4, 5\] but I introduce in the present work a modification of the calculation procedure taking into account that for the peripheral collisions A+A and for p+p collisions in both frameworks; the \(\langle N^p_{\text{part}} \rangle\) and \(\langle N^q_{\text{part}} \rangle\) can not be smaller than two. The nuclear density profile is thus assumed to have a Woods-Saxon form,

\[
n_A(r) = \frac{n_0}{1 + \exp|\sqrt{r^2 - R_n^2}|/d},
\]

where \(n_0\) is the normal nuclear density, \(R_n\) is the nucleus radius and \(d\) is a diffuseness parameter.

For nucleus-nucleus (A+B) collisions, the number of nucleon participants, \(\langle N^p_{\text{part}} \rangle\), is in the present work calculated using the relation,

\[
N^p_{\text{part}}(A+B) = \int d^2s T_A(s)P_{AB}(b)\{1 - \left[1 - \frac{\sigma_{NN}^{\text{inel}} T_B(s-b)}{B}\right]^B\}^A\]

where \(T(b) = \int_{-\infty}^{+\infty} dz n_A(\sqrt{b^2 + z^2})\) is the thickness function and \(P_{AB}(b)\) is defined by:

\[
P_{AB}(b) = \frac{1}{1 - \exp(-\sigma_{NN}^{\text{inel}} T_{AB}(b))} \tag{3}
\]

Fig. 1. Quantitative evaluation of the model calculations expressed as the ratio of the average number of nucleon participants of the PHOBOS Glauber calculations \[13\] to the present work as a function of centrality. Panel a), b) and c) correspond to Au+Au collisions at \(\sqrt{s_{NN}} = 19.6, 62.4\) and 200 GeV, respectively. The gray bands correspond to the systematic errors on the \(\langle N^p_{\text{part}} \rangle\) of PHOBOS Glauber calculations.

Fig. 2. Ratio of \(\langle N^p_{\text{part}} \rangle/\langle N^q_{\text{part}} \rangle\) obtained from the present work presented as a function of the number of nucleon participants for Au+Au collisions at \(\sqrt{s_{NN}} = 19.6, 62.4\) and 200 GeV.
Table 1. Numbers of constituent quark participants, \(N_{q_{\text{part}}}^\text{n}\), obtained from the present work elucidated as a function of collision centrality in Au+Au collisions at \(\sqrt{s_{NN}} = 19.6, 62.4\) and 200 GeV.

| Centrality (%) | 200 GeV | 62.4 GeV | 19.6 GeV |
|----------------|---------|----------|----------|
| 0-3            | 952.5   | 907.2    | 869.4    |
| 3-6            | 837.7   | 796.0    | 761.4    |
| 6-10           | 731.4   | 693.1    | 661.8    |
| 10-15          | 614.5   | 580.4    | 552.8    |
| 15-20          | 501.7   | 472.1    | 448.4    |
| 20-25          | 408.5   | 382.9    | 362.7    |
| 25-30          | 331.6   | 309.7    | 292.6    |
| 30-35          | 265.3   | 246.8    | 232.4    |
| 35-40          | 209.1   | 193.5    | 181.6    |
| 40-45          | 161.6   | 148.8    | 139.1    |
| 45-50          | 123.1   | 112.8    | 105.1    |

Table 2. Values of overlap function TAB and TA for impact parameter \(b=0\) calculated using densities profiles Wood-Saxon and sharp sphere for \(p(A=1)+B\) collisions using the nuclear overlap model.

| profile          | A  | B  | TAB(0)/TA(0) |
|------------------|----|----|--------------|
| Wood-Saxon       | 1  | 236| 0.9          |
| Wood-Saxon       | 1  | 12 | 0.6          |
| sharp sphere     | 1  | 236| 1.0          |
| sharp sphere     | 1  | 12 | 0.9          |

Table 3. Values of \(N_{q_{\text{part}}}^\text{n}\) obtained from the present work for most central and minimum-bias (min-bias) of \(p(\bar{p})+p\) collisions at several collisions energies.

| \(\sqrt{s_{NN}}\) (GeV) | 53 | 200 | 630 | 900 | 1800 |
|-------------------------|----|-----|-----|-----|------|
| \(\sigma_{CQ}/\sigma_{NN}/9\) | 3.89 | 4.66 | 5.33 | 5.44 | 5.66 | 6.22 |
| \(N_{q_{\text{part}}}^\text{n}\) (0-6%) | 4.57 | 4.94 | 5.46 | 5.55 | 5.72 | 5.98 |
| \(N_{q_{\text{part}}}^\text{n}\) (min-bias) | 3.10 | 3.29 | 3.47 | 3.51 | 3.57 | 3.73 |

3 - Physics Results and Discussions

Fig. 3 shows the ratio of \(N_{q_{\text{part}}}^\text{n}\) obtained from the present work elucidated as a function of collisions centrality in Au+Au collisions at \(\sqrt{s_{NN}} = 19.6, 62.4\) and 200 GeV. The \(N_{q_{\text{part}}}^\text{n}\) and \(\langle N_{q_{\text{part}}}^\text{n}\rangle\) from the present work are presented on Table 1 for Au+Au collisions at RHIC energies.

The number of constituent quark participants, \(N_{q_{\text{part}}}^\text{n}\) \(\langle N_{q_{\text{part}}}^\text{n}\rangle\), is calculated in a similar manner by taking into account the following changes related to the physical realities and also taking into account that in peripheral collisions the number of \(\langle N_{q_{\text{part}}}^\text{n}\rangle\) can not be smaller than two:

1. the density is three times that of nucleon density with \(n_0 = 3n_0 = 0.51 \text{ fm}^{-3}\),
2. the cross sections \(\sigma_{CQ} = \sigma_{NN}/9\),
3. the mass numbers of the colliding nuclei are three times their values, keeping the size of the nuclei same as in the case of \(\langle N_{q_{\text{part}}}^\text{n}\rangle\).

Fig. 2 presents the ratio of \(\langle N_{q_{\text{part}}}^\text{n}\rangle/\langle N_{q_{\text{part}}}^\text{n}\rangle\) as a function of \(\langle N_{q_{\text{part}}}^\text{n}\rangle\) for Au+Au collisions at RHIC energies. The ratio shows that the correlation between \(N_{q_{\text{part}}}^\text{n}\) and \(\langle N_{q_{\text{part}}}^\text{n}\rangle\) is not linear and that it depends on the colliding energy.

For proton-proton \((p+p)\) collisions the same procedure has been used to calculate the number of constituent quark participants by using \(A = 3\) and \(B = 3\) and the nuclear density profile is assumed to have a sharp sphere form with uniform radii of 0.8 fm. The reason to use sharp sphere density profile is because the Wood-Saxon density profile becomes unrealistic for low A. The systematic error related to this approximation can be estimated by running the code with \(B=1\) (for \(p+A\)), and comparing obtained TAB(0) value with TA(0) (for impact parameter \(b=0\)). The result is presented in Table 2. The discrepancy is larger for Wood-Saxon profile with low A. The \(N_{q_{\text{part}}}^\text{n}\) for central, 0-6%, and minimum bias of \(p+p\) collisions are presented on the Table 3. Fig. 2 shows the distributions of the number of constituent quark participants obtained from the present work elucidated as a function of collisions centrality for nucleon-nucleon \((p+p)\) collisions at \(\sqrt{s_{NN}} = 53, 200\) and 900 GeV.
production by soft and hard processes. As the beam energy increases, particle production from hard processes, which exceed the number of participants pairs by a factor $\sim 5-6$ in central events for $\sqrt{s_{NN}}$ ranging from 19.6 to 200 GeV, is expected to dominate over that from soft processes as the mini-jets cross sections increase. In the present work, I add to this study an extension the study presented in Ref. [5] from Au+Au at 200 GeV and good scaling of $(dN/d\eta)/(N_{\text{part}}^q)/2$ on centrality for Au+Au at 19.6 and 62.4 GeV. In Fig. 4b, I extend the study presented in Ref. [3] from Au+Au at 200 GeV to 19.6 and 62.4 GeV using the new calculations. I agree with the interpretation presented in Ref. [5] that the experimentally observed increase of $(dN_{ch}/d\eta)|_{|\eta|<1}/(N_{\text{part}}^q)/2$ can be explained by the relative increase in the number of interacting constituent quarks in more central collisions. In the present work, I add to this study $dN_{ch}/d\eta|_{|\eta|<1}$ of $p(\bar{p}) + p$ inelastic as well ND collisions. In Fig. 4b, I observe that the $p(\bar{p}) + p$ data are in good agreement with Au+Au data for different collision centrality at the same energy. It should be noted that in Fig. 4b the $dN_{ch}/d\eta|_{|\eta|<1}$ of $p(\bar{p}) + p$ data (open symbols) have been normalized by minimum-bias $(N_{\text{part}}^q)$ presented in table 3.
In the nucleon participants framework (solid symbols in Fig. 6), the particle density per nucleon participant pair \((N_{ch}^{n}/\langle N_{part}^{n}\rangle/2)\) as open symbols is presented as a function of collision energy. The data are for Au+Au collisions at AGS, Pb+Pb collisions at the CERN-SPS, and for Au+Au and Cu+Cu collisions at RHIC. Also shown for comparison are results from p+p collisions.

In the nucleon participants framework (solid symbols in Fig. 6), the particle density per nucleon participant pair for A+A collisions (solid points) shows an approximately logarithmic rise with \(\sqrt{s_{NN}}\) over the full range of collision energies. The comparison of the particle density per nucleon of Au+Au to Cu+Cu collisions at the same energies, \(\sqrt{s_{NN}} = 62.4\) and 200 GeV indicates that in symmetric nucleus-nucleus collisions the density per nucleon participant does not depend on the size of the two colliding nuclei but only on the collision energy. This means that for Si+Si collisions at \(\sqrt{s_{NN}} = 200\) GeV, the particle density per nucleon participant will be similar to Au+Au collisions at the same energy. Also I observe that the charged particle multiplicity per participant nucleon pair (solid symbols) in A+A collisions is higher compared to p(\(\bar{p}\)) + p collisions at the same energy. It should be noted that number of nucleon participants for p(\(\bar{p}\)) + p has been chosen to be 2 \((N_{part}^{p} / \langle p(\bar{p})\rangle = 2)\).

In contrast, I observe that the charged particle production results from A+A and p+p collisions are similar. It should be noted that Fig 5 is similar to Fig.6 presented in Ref. 11 but it was done independently, extended to the Cu+Cu system, and used the new version of calculation presented in this paper.

In general, the charged particle production in the fragmentation region is thought to be distinct from that at mid-rapidity, although there is no obvious evidence for two separate regions at any of the RHIC energies. This observation is made based on the \(dN_{ch}/dy\) distributions of charged particle presented in Ref. 10,21. Fig. 7 shows the charged particles produced in the fragmentation region for the most central (0-6%) Au+Au collisions at four RHIC energies compared to p(\(\bar{p}\)) + p (inelastic and (NSD)) collisions at 200 GeV. When normalized to \(\langle N_{part}^{n}\rangle/2\), Fig. 7a, I observe that the multiplicity in the limiting fragmentation region in A+A collisions is higher than for p(\(\bar{p}\))+p collisions at the same energy, \(\sqrt{s_{NN}}=200\) GeV. If, however, the comparison is carried out for multiplicities normalized to \(\langle N_{part}^{q}\rangle/2\), Fig. 7b, A+A and p(\(\bar{p}\)) + p collisions exhibit a striking degree of agreement. Again, this observation implies that the number of constituent quark pairs participating in the collision controls the particle production in the central collisions.

4 - Conclusions

The charged particle production results from A+A and p(\(\bar{p}\)) + p collisions have been compared based on the num-
number of nucleon participants and the number of constituent quark participants. In both normalizations, I observe that the charged particle densities in Au+Au and Cu+Cu collisions are similar for both √s_{NN} = 62.4 and 200 GeV. This implies that in symmetric nucleus-nucleus collisions the charged particle density does not depend on the size of the two colliding nuclei but only on the collision energy. In the nucleon participants framework, the particle density at mid-rapidity as well as in the fragmentation region from A+A collisions are higher than those of p(\bar{p}) + p collisions at the same energy. Also the multiplicity of total charged particle, in A+A collisions, as a function of number nucleon participants is higher than p(\bar{p}) + p collisions at the same energy indicating that there is no smooth transition between peripheral A+A and nucleon-nucleon collisions. However, when the comparison is made in the constituent quarks framework, A+A and p(\bar{p}) + p collisions exhibit a striking degree of agreement. The observations presented in this paper imply that the number of constituent quark pairs participating in the collision controls the particle production. One may therefore conjecture that the initial states A+A and p(\bar{p}) + p collisions are similar when the partonic considerations are used in normalization.

I would like to express my gratitude to Bhaskar De for making his code available. This allowed us to cross check his code written in FORTRAN to our code written in C++. The languages of the codes are different but the formula are the same. I would like also to join my gratitude to S. Eremin and S. Voloshin to thank D. Miskowiec for making his code “nuclear overlap model” available. Also I would like to thank M. D. Baker and B. Wosiek for valuable advice concerning the present work. This work was supported by U.S. DOE Grant No. DE-AC02-98CH10886.

References

1. E. Shuryak, Phys. Lett. B496, (2000) 378.
2. E. K.G. Sarkisyan et al., American Institute of Physics 828, (2006) 35.
3. De Bhaskar et al., Phys. Rev. C71, (2005) 024903.
4. R. Nouicer, American Institute of Physics 828, (2006) 11.
5. S. Eremin et al., Phys. Rev. C67, (2003) 064905.
6. D. Kharzeev et al., Nucl. Phys. A730, (2004) 448.
7. I. Arsene et al., Nuclear Physics A757, (2005) 1; K. Adcox et al., Nuclear Physics A757, (2005) 184; B.B. Back et al., Nuclear Physics A757, (2005) 28; J. Adams et al., Nuclear Physics A757, (2005) 102.
8. B. B. Back et al. e-Print arXiv:nucl-ex/0509034.
9. B. B. Back et al., Phys. Rev. Lett. 88, (2002) 22302.
10. R. Nouicer (PHOBOS Collaboration), e-Print arXiv:nucl-ex/0601026.
11. B. B. Back et al., Phys. Rev. C72, (2005) 031901(R).
12. B. Hahn et al., Phys. Rev. 101, (1956) 1131 and C. W. De Jager et al., At. Data Nucl. Data Tables 24, (1974) 479.
13. B. B. Back et al., Phys. Rev. C70, (2004) 021902(R).
14. C. Y. Wong, World Scientific, (1994) 161.
15. M. Gyulassy et al., Comput. Phys. Commun. 83, (1994) 307.
16. L. Ahle et al., Phys. Lett., B476, (2000) 1; Phys. Lett., B490, (2000) 53.
17. J. Bachler et al., Nucl. Phys., A661, (1999) 45.
18. C. Blume et al., Proceeding of QM, (2001).
19. G. Roland (PHOBOS Collaboration), e-Print arXiv:nucl-ex/0510042.
20. F. Abe et al., Phys. Rev., D41, (1990) 2330.
21. B. B. Back et al., Phys. Rev. Lett., 91, (2003) 052303.
