Influence of collisional rate coefficients on water vapour excitation

F. Daniel¹, J. R. Goicoechea¹, J. Cernicharo¹, M.-L. Dubernet²³, and A. Faure⁴

¹ Departamento de Astrofísica, Centro de Astrobiología, CSIC-INTA, Ctra. de Torrejón a Alcalvín km 4, 28850 Madrid, Spain
e-mail: danielf@cab.inta-csic.es
² Observatoire de Paris, LUTH UMR CNRS 8102, 5 place Janssen, 92195 Meudon, France
³ Université Pierre et Marie Curie, LPMMA UMR CNRS 7092, Case 76, 4 place Jussieu, 75252 Paris Cedex 05, France
⁴ UJF-Grenoble 1/CNRS-INSU, Institut de Planétologie et d’Astrophysique de Grenoble (IPAG) UMR 5274, 38041 Grenoble, France

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Abstract

Context. Water is a key molecule in many astrophysical studies that deal with star and planet forming regions, evolved stars, and galaxies. Its high dipole moment makes this molecule subthermally populated under the typical conditions of most astrophysical objects. This motivated calculation of various sets of collisional rate coefficients (CRC) for H₂O (with He or H₂), which are needed to model its rotational excitation and line emission.

Aims. The most accurate set of CRC are the quantum rates that involve H₂. However, they have been published only recently, and less accurate CRC (quantum with He or quantum classical trajectory (QCT) with H₂) were used in many studies before that. This work aims to underline the impact that the new available set of CRC have on interpretations of water vapour observations.

Methods. We performed accurate non-local, non-LTE radiative transfer calculations using different sets of CRC to predict the line intensities from transitions that involve the lowest energy levels of H₂O (E < 900 K). The results obtained from the different CRC sets were then compared using line intensity ratio statistics.

Results. For the whole range of physical conditions considered in this work, we find that the intensities based on the quantum and QCT CRC are in good agreement. However, at relatively low H₂ volume density (n(H₂) < 10⁻⁴ cm⁻³) and low water abundance (χ(H₂O) < 10⁻³), which corresponds to physical conditions relevant when describing most molecular clouds, we find differences in the predicted line intensities of up to a factor of ~3 for the bulk of the lines. Most of the recent studies interpreting early Herschel Space Observatory spectra have used the QCT CRC. Our results show that, although the global conclusions from those studies will not be drastically changed, each case has to be considered individually, since depending on the physical conditions, the use of the QCT CRC may lead to a mis-estimate of the water vapour abundance of up to a factor of ~3. Additionally, the comparison of the quantum state-to-state and thermalised CRC, including the description of the population of the H₂ rotational levels, show that above Tₖ ~ 100 K, large differences are expected from those two sets for the p–H₂ symmetry. Finally, we find that at low temperature (i.e. Tₖ < 100 K) modelled line intensities will be differentially affected by the symmetry of the H₂ molecule. If a significant number of H₂O lines is observed, it is then possible to obtain an estimate of the H₂ ortho-to-para ratio from the analysis of the line intensities.

Key words. line: formation – molecular data – radiative transfer – radiation mechanisms: thermal – ISM: abundances – ISM: molecules

1. Introduction

Water is a key molecule for both the chemistry and the cooling budget along the star formation trail. Determining the water vapour abundance is a long-standing problem in astrophysics. Because water vapour is predicted to be an abundant molecule in the gas phase, determining its spatial extent, its distribution, and its abundance is crucial for modelling the chemistry and the physics of molecular clouds, comets, evolved stars, and galaxies (Neufeld & Kaufman 1993; Neufeld et al. 1995; Cernicharo & Crovisier 2005; van Dishoeck et al. 2011). In warm molecular clouds, water vapour can play a critical role in the gas cooling (Neufeld & Kaufman 1993; Neufeld et al. 1995), hence in the evolution of these objects.

Unfortunately, water is an abundant molecule in our atmosphere, making it particularly difficult to observe its rotational lines and vibrational bands from Earth. Even so, some observations of H₂O maser lines have been performed from ground-based and airborne telescopes: the 616–523 at 22 GHz (Cheung et al. 1969), the 515–422 at 325 GHz (Menten et al. 1990a), the 1029–936 at 321 GHz (Menten et al. 1990b), and the 313–220 at 183.31 GHz (Waters et al. 1980; Cernicharo et al. 1990, 1994). The spectrometers on board the Infrared Space Observatory (Kessler et al. 1996) provided a unique opportunity to observe infrared (IR) H₂O thermal lines in a wide variety of astronomical environments.

Several studies have demonstrated that water emission is a unique tracer of the warm gas and energetic processes taking place during star formation (see review by van Dishoeck 2004; Cernicharo & Crovisier 2005). In particular, ISO observations show that far-IR H₂O emission lines are important coolants of the warm gas affected by shocks (e.g., more than 70 pure rotational lines were detected towards Orion KL outflows; Cernicharo et al. 2006a) confirming earlier theoretical predictions of its importance in the shocked gas cooling (e.g., Neufeld & Kaufman 1993). ISO also detected widespread H₂O absorption towards the Galactic centre (e.g., Goicoechea et al. 2004) and towards the nucleus of more distant galaxies (e.g., González-Alfonso et al. 2004). After ISO, the launch of both the Submillimeter Wave Astronomy Satellite, SWAS (Melnick et al. 2000), and ODIN (Nordh et al. 2003) allowed observation of the 1₁₀–1₁₀₁ fundamental transition of both H₂O (at 557 GHz)
and H$_{2}$O (at 548 GHz, first detected by the Kuiper Airborne Observatory; Zmuidzinas et al. 1995) at high heterodyne spectral resolution but poor angular resolution. Their resolved line profiles (line-wing emission, widths, self-absorption dips, etc.) have been studied in detail. Finally, the Spitzer Space Telescope has detected even higher excitation H$_2$O pure rotational lines (up to $E_u = 3000$ K) in the shocked gas around protostars (albeit at low spectral resolution; e.g., Watson et al. 2007).

The HIFI and PACS spectrometers on board Herschel Space Observatory (Filbratt et al. 2010) provide much higher sensitivity and angular resolution than previous far-IR observations, allowing us to detect a larger number of excited H$_2$O lines in many more sources and to better constrain the spatial origin of the water vapour emission. The HIFISTARS1 key project has addressed the problem of the water abundance in evolved stars and complement with high spectral resolution the results obtained previously by ISO. Similar goals have been addressed by the MESS (Mass-loss of Evolved Star$^2$) key project, but it covers a much larger spectral domain with lower spectral resolution. The WISH (Water In Star-forming regions with Herschel$^1$) key project focussed on the study of young stellar objects in different evolutionary stages. Early Herschel results include the detection of strong H$_2$O emission in protostellar environments (e.g., van Dishoeck et al. 2011), the presence of water vapour in diffuse interstellar clouds with an ortho-to-para ratio (OTPR) consistent with the high temperature ratio of 3 (Li et al. 2010), the detection of cold water vapour in TW Hydrae protoplanetary disk with a low OTPR of ≈0.8 (Hogerheijde et al. 2011), and the widespread occurrence of H$_2$O in circumstellar envelopes around O-rich and C-rich evolved stars (Royer et al. 2010; Neufeld et al. 2011). In the outflows of Class 0 protostars, for example, ture of pure rotational lines of water vapour (up to $9_{18}$–$9_{09}$ or $E_u = 1500$ K) are readily detected in the far-IR domain (Herczeg et al. 2012; Goicoechea et al. 2012).

To derive the water vapour abundance and to estimate the prevailing physical conditions in the above environments, the energy-level excitation and the radiative transfer (RT) of H$_2$O lines has to be understood. H$_2$O is an asymmetric molecule with a large high dipole moment makes most of its transitions to be subthermally excited (see, e.g., Cernicharo et al. 2006b), harbouring very high opacities (see, e.g., González-Alfonso et al. 1998), many of them being maser in nature (Cheung et al. 1969; Waters et al. 1980; Phillips et al. 1980; Menten et al. 1990a,b; Menten & Melnick 1991; Cernicharo et al. 1990, 1994, 1996, 1999, 2006b; González-Alfonso et al. 1995, 1998). In addition to a good description of the source structure, accurate modelling thus requires the availability of accurate collisional rate coefficients (CRC). In the case of saturated masers, a special formalism has to be developed to take saturation effects into account and to solve the RT problem (Daniel & Cernicharo 2012). To summarise, the water vapour abundance in different environments can change by orders of magnitude (e.g., van Dishoeck et al. 2011), and H$_2$O rotational line profiles are sensitive probes of the gas kinematics and physical conditions (e.g., Kristensen et al. 2012). These facts make water-vapour lines a powerful diagnostic tool in astrophysics.

The methodology used to compare two CRC sets is presented in Sect. 2, and a comparison between the various sets available for H$_2$O is given in Sect. 3. A discussion of the effect introduced by the H$_2$ OTPR is presented in Sect. 4. Finally, we discuss the current results in Sect. 5, and the conclusions are drawn in Sect. 6.

2. Comparison between collisional rate coefficients sets: methodology

Water is a key molecule for both the chemistry and cooling budget of the warm molecular gas. The need to understand the excitation mechanisms leading to line formation motivated the determination of various CRC sets for this molecule.

The first water-vapour CRC were calculated using He as a collisional partner, considered the first 45th rotational energy levels for both ortho- and para-H$_2$O, and they were calculated for temperatures in the range 20–2000 K (Green et al. 1993). Collisions with H$_2$ were subsequently determined (Phillips et al. 1996) making use of the 5D potential energy surface (PES) described in Phillips et al. (1994). This study showed that considering either ortho- or para-H$_2$ as a collisional partner could lead to substantial differences in the magnitude of the CRC. However, this study dealt with a limited number of H$_2$O energy levels (5 levels), and results were only made available for a reduced range of temperatures (20–140 K). The latter calculations were extended to lower temperatures (to cover the range 5–20 K) by Dubernet & Grosjean (2002) and Grosjean et al. (2003) by making use of the same PES. The importance of water subsequently led to calculating of a high-precision 9D PES for the H$_2$O – H$_2$ system (Faure et al. 2005; Valirom et al. 2008). The influence of the results based on the latter PES (averaged over the vibration of H$_2$O and H$_2$) thus reducing the dimension to 5 with the previous PES (Phillips et al. 1994) are discussed in Dubernet et al. (2006). Using the latter PES, quantum-classical trajectory (QCT) calculations were performed to determine CRC for the 45th first energy levels of H$_2$O for both ortho- and para-H$_2$ (Faure et al. 2007). The range of temperature covered by these calculations is 100–2000 K (CRC are provided below 100 K, making use of the quantum CRC of Dubernet et al. 2006, for the transitions that involve the lowest five energy levels of either o–H$_2$O or p–H$_2$O and assuming a constant temperature dependence for the other transitions). Making use of laboratory measurements for the vibrational relaxation of water and QCT calculations (Faure et al. 2005), the QCT CRC of Faure et al. (2007), obtained for the vibrational ground state, have subsequently been scaled to provide ro-vibrational CRC for the first five vibrational states (Faure & Jesselin 2008). Finally, quantum calculations were performed for the H$_2$O – H$_2$ system that make use of the same 5D PES as the one used in the QCT calculations. These quantum calculations provide CRC for the first 45 energy levels of both ortho and para H$_2$O and for temperatures covering the 5–1500 K range (Dubernet et al. 2009; Daniel et al. 2010, 2011). In these studies, emphasis is on including the excited energy levels of H$_2$. Therefore, apart from the usual state-to-state (STS) CRC commonly calculated in quantum studies (i.e. with H$_2$ remaining in

\footnote{1 http://hifistars.oan.es/}

\footnote{2 http://www.univie.ac.at/space/MESS/}

\footnote{3 http://www.strw.leidenuniv.nl/WISH/}

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its fundamental rotational level during the collision), the availability of the information relative to the H₂ excitation is used to determine thermalised CRC.

Owing to the time at which the different CRC sets were made available and owing to the number of energy levels considered and to the temperature coverage, analysis of water excitation has mainly been based on three sets: the quantum H₂O – He CRC of Green et al. (1993), the QCT CRC of Faure et al. (2007), and the quantum CRC of Dubernet et al. (2006, 2009) and Daniel et al. (2010, 2011). In what follows, we discuss the H₂O line intensity predictions based on these three CRC sets and calculated with a precise non-LTE non-local radiative transfer code. Additionally, we focus the discussion on the o–H₂O symmetry, since the results are similar for the p–H₂O symmetry.

2.1. Radiative transfer modelling

We performed RT calculations using the various sets of CRC available for o–H₂O and p–H₂O. The numerical code used to solve the molecular excitation and the RT problem is described in Daniel & Cernicharo (2008). The water vapour spectroscopic parameters, i.e. line frequencies and Einstein coefficients, are taken from the HITRAN database (Rothman et al. 2009). The model consists of a static spherical homogeneous cloud with turbulence velocity dispersion fixed at 1 km s⁻¹ and with a radius of ∼4.5 × 10¹⁶ cm (i.e. 6'' at 500 pc). Since we focus on collisional effects, pumping by the dust IR radiation is not included in the first stage, so that the population of the water energy levels is determined by the collisions with the H₂ molecules and to radiative trapping due to line opacity effects. The inclusion of dust emission is, however, briefly discussed in Sect. 5. A grid of models has been run, leaving the gas temperature, the H₂ volume density, and the water abundance relative to H₂ as free parameters. Those quantities vary in the ranges \( T_K \in [200 \text{ K}; 1000 \text{ K}], n(H_2) \in [10^5; 2 \times 10^9] \text{ cm}^{-3} \) and \( \chi(H_2O) \in \{10^{-8} ; 10^{-6} ; 10^{-4}\} \), for both o–H₂O and p–H₂O. All the RT models are performed considering the first 45th energy levels of p–H₂O or o–H₂O, irrespective of the CRC set used.

Since we solve the non-local excitation problem, we consider an average of the parameters that describe the radiative transitions in order to compare the results based on the different CRC sets. Therefore, the influence of the CRC on the line emission is estimated from the quantity:

\[
I_j = B(T_{bg}) \epsilon^{-(r_i)} + B(T_{ex}) \times (1 - \epsilon^{-(r_i)})
\]

where \( B(T) \) stands for the Planck function, \( \tau_j \) for the opacity at the \( j \) line centre, and \( T_{bg} \) is the temperature of the background radiation (set to the CMB temperature in what follows, except if specified). Here, \( I_j \) corresponds to the specific intensity of the transition \( j \), along a ray with constant excitation conditions (i.e. constant \( T_{ex} \)). The excitation temperature \( T_{ex} \) is defined as an average over the \( N \) radial grid points of the models, and is calculated according to

\[
T_{ex} = \frac{\mathcal{A}}{2} \sum_{i=1}^{N-1} \left[ \kappa(r_i) T_{ex}(r_{i+1}) + \kappa(r_{i+1}) T_{ex}(r_{i+1}) \right] \times \frac{r_{i+1} - r_i}{r_N - r_1}
\]

where \( r_i \) stands for the distance of the \( i \)th grid point to the centre of the sphere, \( \mathcal{A} \) is a normalisation coefficient, and \( \kappa(r) \) is the line absorption coefficient at radius \( r \). Calculating \( T_{ex} \) this way, we prevent lines with suprathermal excitation (i.e. \( T_{ex} > T_K \)), but with nearly equal populations for the upper and lower levels, from having their averaged \( T_{ex} \) overestimated. Indeed, even

\[
\tau_j = \frac{1}{2} \sum_{i=1}^{N-1} \left[ \kappa(r_i) + \kappa(r_{i+1}) \right] \times (r_{i+1} - r_i).
\]

The various models are compared using \( I_j \) rather than the line intensity peaks (noted \( \text{max}(I_j) \)) in what follows or the integrated area of the lines (noted \( W_j \)), for various reasons. At first glance, the last two estimators would be more natural, since such quantities would be the ones used to compare observations and models. However, a difficulty arises because for a given line, the line profiles may differ from one model to the next. In such a case, the ratio obtained considering either \( \text{max}(I_j) \) or \( W_j \) can differ by a few tens of percentage points.

This is illustrated in Fig. 1, where the models considered correspond to the physical parameters \( T_K = 800 \text{ K}, n(H_2) = 2 \times 10^7 \text{ cm}^{-3} \) and \( \chi(\text{o-H}_2\text{O}) = 10^{-6} \). The collisional partner is p-H₂,

![Fig. 1. Comparison of the line intensity ratios based on three estimators: \( I_j \), the integrated area \( W_j \), or the peak intensity \( \text{max}(I_j) \) (see text for details). The four upper panels give the brightness temperature of a few o–H₂O lines. The black curve corresponds to the profile obtained with the quantum CRC set and the red curves to the QCT CRC set (see text for details). In the latter case, the profile is scaled according to the ratios of \( I_j \) (plain curve), \( W_j \) (dashed curve), or \( \text{max}(I_j) \) (dotted curve) so that the profiles that are plotted would correspond to a ratio of unity according to the three estimators. The two bottom panels represent the variations in the ratios obtained between the various indicators and for all the lines of the model.](image-url)

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and the results being compared are obtained using the QCT CRC of Faure et al. (2007) and STS quantum CRC of Dubernet et al. (2009) (respectively labelled QCT and quant. in the following). These CRC sets are more extensively discussed in Sect. 3. The two bottom panels show the variation in $W_j^{\text{quant.}} / W_j^{\text{QCT}}$ (left panel) and $\max(I_j)^{\text{quant.}} / \max(I_j)^{\text{QCT}}$ (right panel) as a function of $I_j^{\text{quant.}} / I_j^{\text{QCT}}$. Considering the integrated intensity, it can be seen that most of the $W_j$ and $I_j$ ratios show maximum differences of the order of $25\%$. The two dashed lines in the left panel correspond to straight lines of slopes 0.75 and 1.25, so they delimit a maximum deviation of $25\%$. Considering the peak intensity (right panel), it can be seen that the correlation between the $\max(I_j)$ and $I_j$ ratios is better than for the case of the integrated intensity. In that case, the maximum differences are lower than $10\%$. The dashed lines correspond to straight lines of slopes 0.9 and 1.1. The four upper panels illustrate that the three estimators start to lead to different ratios when the line profiles of the two models differ. In this figure, we report the brightness temperature for the impact parameter that crosses the centre of the sphere. The profile obtained with the p–H$_2$ QCT CRC corresponds to the black curves. The red curves correspond to the profiles obtained with the p–H$_2$ quantum CRC, and scaled by the ratio $I_j^{\text{QCT}} / I_j^{\text{quant.}}$, $W_j^{\text{QCT}} / W_j^{\text{quant.}}$, and $\max(I_j)^{\text{QCT}} / \max(I_j)^{\text{quant.}}$. In other words, the red curves would correspond to line profiles that would lead to a ratio of unity, when compared to the black curve and depending on the estimator used. It can be seen that for the 3$\alpha$–3$\gamma_1$ line, since the line profiles derived from the two CRC sets are identical, the ratio obtained from the three estimators are identical, too. On the other hand, for example for the 3$\gamma_2$–3$\gamma_1$ line, the three estimators lead to different ratios since the line profiles obtained using the two CRC sets differ.

Finally, we emphasise that, in principle, any of the three estimators could be used in order to perform the comparisons presented in the next sections. The conclusions would not be affected by this choice thanks to the good correlation between the ratios obtained with those three estimators. We prefer to use $I_j$ because of its simplicity and because it reduces the line intensity simply to two parameters, the averaged excitation temperature and the line opacity, the first quantity being a useful indicator of how far the line is from thermalization.

### 2.2. Comparison of rate coefficient sets

To compare two CRC sets, noted SET1 and SET2, we consider the values taken by the ratios $x_j = I_j^{\text{SET1}} / I_j^{\text{SET2}}$, where $I$ is defined by Eq. (1) and where the index $j$ stands for the $j$th radiative transition. The comparisons are made considering the statistics on the $M$ radiative lines that respect the criteria:

- the line does not show substantial population inversion (i.e., we adopt as a selection criterion that the opacity of a line in the inverted region cannot be greater than 0.5% of the opacity of the line in the thermal region.)
- the upper level of the line has an energy below the $N$th level (labelled as $N_{\text{max}}$ in what follows)
- the intensity of the line as given by Eq. (1) is above 10 mK.

The first criterion means that the masers are discarded from the statistical analysis. The following conclusions therefore do not concern the lines observable with the ALMA interferometer. We refer to Daniel & Cernicharo (2012) for a discussion concerning the impact of the CRC on these maser lines. From these $M$ lines, we define the mean (denoted $m$) and standard deviation (denoted $\sigma$) associated to the $x_j$ ratios, the latter quantity being given by

$$\sigma = \sqrt{\frac{1}{M} \sum_{j=1}^{M} (x_j - m)^2}.$$  \hspace{1cm} (4)

Additionally, we discuss the results using the normalised standard deviation defined as $\sigma/m$ rather than $\sigma$.

### 3. Comparison between various H$_2$O CRC

In what follows, we discuss the H$_2$O line intensity predictions based on the three CRC sets that have been widely used, i.e. the quantum H$_2$O$\rightarrow$He CRC of Green et al. (1993), the QCT CRC of Faure et al. (2007), and the quantum CRC of Dubernet et al. (2006, 2009) and Daniel et al. (2010, 2011).

#### 3.1. o–H$_2$O QCT and quantum STS CRC with H$_2$ compared to quantum He CRC

In this section, various comparisons are made between the quantum STS CRC calculated with either p–H$_2$ (Dubernet et al. 2009; Daniel et al. 2011) or o–H$_2$ (Daniel et al. 2011), the quantum STS CRC calculated with He (Green et al. 1993), and the QCT calculations (Faure et al. 2007). When referring to the quantum H$_2$ STS CRC, it is assumed that the CRC stands for the CRC where H$_2$ remains in its fundamental rotational energy level (i.e. either $j_2 = 0$ for p–H$_2$ or $j_2 = 1$ for o–H$_2$ with $j_2$ being the H$_2$ rotational quantum number). We note that QCT rate coefficients are not STS, but were obtained for thermal populations of p–H$_2$ and o–H$_2$; i.e., they are thermalised CRC (see below). In the RT calculations, the CRC calculated with He are scaled according to the differing reduced masses of the H$_2$O–He and H$_2$O–H$_2$ systems to emulate collisions with H$_2$.

#### 3.1.1. p–H$_2$ rate coefficients

A first comparison is made between the o–H$_2$O / p–H$_2$ CRC sets obtained with the quantum calculations and the QCT calculations, both with respect to the quantum calculations performed with He. The mean and normalised standard deviations of the ratios $P_j^{\text{He}} / P_j^{\text{QCT}}$ are represented in Fig. 2 for various water abundances and by considering the o–H$_2$O lines with upper energy levels below the 20th level ($E_n < 900$ K). It appears that the behaviour of the $x_j$ ratios can be distinguished between two regimes, which are separated by a threshold (noted $n$ in what follows) in the water volume density $n$(H$_2$O) $= n$(H$_2$) $\times$ (H$_2$O). For water volume densities $n$(H$_2$) $\times$ (H$_2$O) $> n$, the mean value is around 1 and the normalised standard deviation takes low values (typically below 0.1). This corresponds to the thermalised regime where the line intensity ratios are basically independent of the adopted CRC set. In this regime, most of the lines show large optical depths. These depths imply that the critical densities of the lines become lower than in the optically thin limit, hence producing the thermalization of the level populations. For $n$(H$_2$) $\times$ (H$_2$O) $< n$, the level populations are determined by both collisional and radiative processes, making the mean value differ from one and leading to an increase in the normalised standard

\footnote{I.e. $n_c = A_E(\beta) / C_{\text{H}_2}$ where $\beta$ is the probability that a photon escapes the medium; with $\beta = 1$ in the optically thin case and $\beta \sim 1/\tau$ when the line becomes optically thick.}
In what follows, this regime is referred as subthermal regime.

In Fig. 2 we show a comparison of the line intensity ratios obtained with the quantum p–H₂ CRC (left column) and QCT p–H₂ CRC (right column), both compared to the quantum He CRC. Examining the p–H₂ CRC, we see that independently of the abundance considered, the mean value is in the range $0.45 < m < 1.35$. The normalised standard deviation is below 0.5 for all the free parameter space, which means that most of the lines (roughly 70% of the lines considered) show deviations of less than 50% around the mean value. In other words, the main effect introduced by considering the H₂ CRC will be to scale the line intensities with respect to the intensities derived from the He CRC. The maximum difference in the scaling factor is encountered at high temperature and low H₂ volume densities, where the line intensities based on the H₂ CRC are found to be
lower by a factor around ~2, for \( \chi(\text{H}_2\text{O}) = 10^{-8} \). Additionally, the relative line intensities are expected to vary from one set to the other, with maximum variations of the order of 50% for the bulk of the lines.

The QCT calculations show slightly larger differences, as expected since they correspond to thermalised CRC. Indeed, we find that irrespective of the water vapour abundance, the mean value of the ratios is in the range \( 1 < m < 2.9 \), for the whole parameter space considered here. The normalised standard deviation can take values of up to ~0.7. The spread of the ratio around the mean value is of the same order as the one found for the quantum p-H\(_2\) CRC.

In Fig. 4 (right column), we show a direct comparison of the results predicted by the STS and QCT CRC. Independently of the water abundance, the QCT CRC predict higher intensities (a factor 2 higher) than the STS CRC. This is because the QCT calculations are a thermal average over the H\(_2\) energy levels and because of the large differences of the CRC for H\(_2\) in its fundamental state \( j_2 = 0 \) and in the \( j_2 = 2 \) state. This is discussed further when considering the thermalised CRC (see Sect. 3.2).

### 3.1.2. \( \text{H}_2 \) rate coefficients

A second comparison concerns the results obtained with \( \text{H}_2 \) as a collisional partner. The results obtained with the quantum and QCT CRC are compared to the results obtained with He in Fig. 8. Not surprisingly, the H\(_2\) quantum and QCT calculations compares closely to the results obtained with He. The main effect concerns the overall scaling of the ratios. In the subthermal regime, the intensity ratios obtained using \( \text{H}_2 \) are higher than the one obtained using He, irrespective of the water abundance. A typical increase of 50% is found for the intensity of the lines, with mean values that can be higher than three in the regime of low temperatures and low densities. This result is expected from a direct consideration of CRC obtained with \( \text{H}_2 \). Indeed, these rates are typically higher than the rates with He, by factors of up to a factor 10, so the water energy levels are more easily populated when considering \( \text{H}_2 \) as a collisional partner. This results in brighter lines. Additionally, we note that the normalised standard deviation is high, and its variations are correlated with the variations in the mean value; i.e., the higher the mean value, the higher the normalised standard deviation.

A direct comparison of the results obtained with the quantum and QCT calculations is shown in Fig. 4 for \( \text{H}_2 \) (left column). The differences found for the intensities are modest as long as the water abundance is such that \( \chi(\text{H}_2\text{O}) \geq 10^{-6} \). In that case, the mean value is found to be around one, and the normalised standard deviation is below 0.3 for all the parameter space. The main differences are found for \( n(\text{H}_2) < 10^{17} \text{ cm}^{-3} \) and \( \chi(\text{H}_2\text{O}) \sim 10^{-8} \text{ cm}^{-3} \) where mean values in the range \( 1.5 < m < 2 \) are obtained.

### 3.2. Quantum thermalised CRC with QCT or STS CRC

In this section, we compare the intensities predicted using the quantum STS CRC with the one derived using the thermalised CRC (both defined in Dubernet et al. 2009; Daniel et al. 2011), defined as

\[
R_{ij} = \sum_{j_2} n(j_2) \sum_{j_1} C_{ij}(j_2 \rightarrow j_1).
\]

In this expression, \( C_{ij}(j_2 \rightarrow j_1) \) stands for the STS CRC from state \( i \) to state \( j \) for the H\(_2\)O molecule, and it corresponds to the transition \( j_2 \rightarrow j_1 \) for the H\(_2\) molecule. These thermalised CRC thus consider the possibility of energy transfer for both the target molecule (H\(_2\)O in the present case) and the collider. The populations of the H\(_2\) energy levels (noted \( n(j) \)) in the above expression) are assumed to be in thermal equilibrium, so that the populations are given by the Boltzmann distribution. In principle, any astrophysical study should consider thermalised rather than STS CRC when dealing with line excitation. In practice, the H\(_2\)O molecule (and its isotopomers in Faure et al. 2012) is the only molecule for which thermalised CRC have been calculated with a quantum approach. In what follows, we emphasise the effects introduced by considering thermalised rather than STS CRC, keeping in mind that the current findings obtained for the case of water vapour can be extrapolated to other molecules.

The thermalised CRC differ from the quantum STS CRC in two ways. In the following discussion, we consider the case of the collisions with p-H\(_2\). At low temperature (i.e. \( T_K \leq 50 \text{ K} \)), only the fundamental level of the p-H\(_2\) molecule is substantially populated. The thermalised CRC thus reduce to \( R_{ij} \sim C_{ij}(0 \rightarrow 0) + C_{ij}(0 \rightarrow 2) \).

At low temperature, the second term of this expression is often negligible compared to the first term, except for the H\(_2\)O transitions for which the variation in the energy induced by the collision is higher than the energy needed to excite the p-H\(_2\) molecule to its first excited state. In the case of p-H\(_2\), this corresponds to transitions that satisfy \( \Delta E_{ij} > 500 \text{ K} \). For these transitions, the term \( C_{ij}(0 \rightarrow 2) \) starts to be dominant in the evaluation of the thermalised CRC since such a rate can be higher by up to a factor 10 in comparison to the STS CRC where H\(_2\) remains at its fundamental level. The main effect induced by this process is to efficiently populate the H\(_2\)O energy levels for the levels with energies higher than 500 K. This is illustrated in Fig. 5, for a model with parameters \( n(\text{H}_2) = 10^6 \text{ cm}^{-3} \), \( T_K = 50 \text{ K} \), and \( \chi(\text{H}_2\text{O}) = 10^{-4} \). In this figure, we report the water vapour-level populations averaged over radius. It can be seen that for the levels with energies below 500 K, the STS and thermalised CRC give similar results for the level populations. On the other hand, for the levels with energies higher than 500 K, the populations obtained using the thermalised CRC are generally ten times higher than the one obtained from the STS CRC. In the case of low temperatures, these differences are irrelevant for any astrophysical study since the levels higher than 500 K correspond to transitions that are far below the detection limit of the current telescopes. This example is, however, given to emphasise the effect introduced by the term \( C_{ij}(0 \rightarrow 2) \), the same effect being found at higher temperatures. However, at higher temperatures, the transitions from the \( j_2 = 2 \) state make the influence of those terms less evident when considering the level populations, as discussed below.

At higher temperature, the first p-H\(_2\) excited state starts to be substantially populated. Collisions from the state \( j_2 = 2 \) thus influence the evaluation of the thermalised CRC. In this case, all the H\(_2\)O transitions are affected by the scaling of the CRC due to the term \( n(j_2 = 2) \times C_{ij}(2 \rightarrow 2) \). In the case of the H\(_2\)O molecule, the term \( C_{ij}(2 \rightarrow 2) \) is generally larger than \( C_{ij}(0 \rightarrow 0) \) by a factor that ranges from two to ten depending on the transition. Consequently, the thermalised CRC for all the transitions are increased overall since at the temperatures of 100, 200, 500 K, the population of the \( j_2 = 2 \) state accounts for 3, 28, and 58% of the total p-H\(_2\) molecules, respectively. As an example, at 200 K, all the thermalised CRC are increased by factors in the range 1.5–3.5 depending on the transition. Additionally, as discussed in the case of the low temperatures, the CRC for the transitions with \( \Delta E_{ij} > 500 \text{ K} \) will be increased due to the term \( C_{ij}(0 \rightarrow 2) \).
Finally, Fig. 6 shows a comparison of the results based on thermalised and STS CRC, for temperatures in the range 20–100 K and for the first ten o–H₂O rotational energy levels. From this figure, it appears that the temperature at which the thermalised CRC start to influence the line intensities is around \( T_K \sim 60 \text{ K} \).

3.2.1. Comparison of the thermalised, STS, and QCT CRC

In Fig. 7, we compare the quantum STS (Dubernet et al. 2009; Daniel et al. 2011) and QCT (Faure et al. 2007) CRC with the results obtained with the thermalised CRC for p–H₂ (Dubernet et al. 2009; Daniel et al. 2011). It can be seen that adopting the thermalised CRC strongly influences the results. Indeed, in the limit of low density (i.e. \( n(\text{H}_2) \sim 10^7 \text{ cm}^{-3} \)), both STS and QCT CRC give results that can differ by more than a factor 3, if we consider the mean value. Such high differences are found over all the temperatures considered here for what concerns the STS CRC. On the other hand, the differences between the QCT and thermalised CRC decrease with temperature. Above 400 K, the mean value obtained from the comparison of the QCT and thermalised CRC is below two.
Fig. 4. Comparison of the results based on the quantum CRC from Dubernet et al. (2009) and Daniel et al. (2011) with the QCT CRC from Faure et al. (2007), for both $o$–H$_2$ (left column) and $p$–H$_2$ (right column).

In Fig. 8, we compare the results based on thermalised and STS (Daniel et al. 2011) CRC for the $o$–H$_2$ symmetry. In this figure, we see that the thermalised CRC give similar results as the STS CRC, with a mean value in the range $1 < m < 1.2$ and normalised standard deviation below 0.15 for all the parameter space. The results are shown for a water abundance $\chi$(H$_2$O) = $10^{-8}$, but the results are similar for other abundances. The similarity of the derived line intensities is because the terms $C_{ij}(j_2 \rightarrow j'_2)$ that involve the $j_2 = 1$ state or $j_2 = 3$ state are similar in magnitude.

Figure 9 show the $I_{\text{HER}}/I_{\text{QCT}}$ ratios for both $o$–H$_2$ and $p$–H$_2$, for eight H$_2$O transitions commonly observed with the HIFI and PACS spectrometers onboard Herschel. For each line, the ratios for the prediction based on the $o$–H$_2$ set are given in the left-hand panel, while the ratios obtained from the CRC that involve $p$–H$_2$ are given in the right one. We note the similarity of the intensity ratio obtained for both the $o$–H$_2$ and $p$–H$_2$ symmetries. This behaviour is discussed further in Sect. 4. The figure corresponds to a water abundance $\chi$(H$_2$O) = $10^{-8}$, and it appears that the two CRC sets will lead to qualitatively similar predictions for the line.
intensities. Indeed, the maximum variations which are found are close to 3, in the worst case. For the lines considered here, and considering collisions with o–H₂ (the most abundant symmetry for H₂ in hot gas), the o–H₂O lines that show the largest differences (i.e. greater than a factor of ~2) are the 1₁₀–1₀₁, 2₂₁–2₁₂, 3₃₀–2₃₁ lines. These differences are found at \( n(\text{H}_2) < 10^4 \text{ cm}^{-3} \) for all the temperatures considered here. On the other hand, some lines show only small variations from one temperature to another, with intensities that agree within 20\% (e.g. 2₁₂–1₀₁, 3₀₃–2₁₂, 3₁₂–3₀₁; 4₁₄–3₀₃). Moreover, we find that for the majority of the lines, the predictions based on the QCT CRC give lower intensities for the o–H₂ symmetry (for all the lines except the 3₁₂–3₀₁ for which a ratio between 0.6 and 0.8 is found at high temperatures). This implies that an analysis based on the QCT CRC will tend to underestimate the water abundance.

3.2.2. Behaviour of the thermalised CRC

A striking feature when considering the comparison of the STS and thermalised CRC arises from the behaviour at low temperature. Indeed, the greatest differences are found in the range 200–400 K between those sets. Simply considering that the population of the p–H₂ J = 2 level increases with temperature, one would expect the differences between those two sets to behave similarly, to reach a maximum when the fundamental level is depopulated. On the contrary, the highest differences are found around 200 K and tend to diminish while the temperature increases. This effect is due to the terms \( C_{ij}(J_f \rightarrow J_i) \) with \( \Delta J_2 \geq 2 \). In order to quantify the influence of those terms, we used an ad hoc set of CRC. In this set, the thermalised CRC are calculated setting all the CRC with \( \Delta J_2 \neq 0 \) to 0. The comparison between the results based on the STS, QCT, and thermalised CRC with this ad hoc set is shown in Fig. 10. The comparison is made at a density \( n(\text{H}_2) = 2 \times 10^7 \text{ cm}^{-3} \) and for a water abundance \( X(\text{H}_2\text{O}) = 10^{-6} \). The choice of these parameters is based on the results shown in Fig. 7, where it can be seen that for both the QCT and STS CRC, these parameters correspond to the maximum differences encountered. Considering the mean value obtained for the ratio \( P^{\text{QCT}} / P^{\text{approx}} \), we find that it has a constant value close to 1.0 over the whole temperature range. The normalised standard deviation decreases from 0.4 to 0.3 as the temperature increases. In other words, the ad hoc set of CRC and the QCT CRC gives the same results within ~30\%. This shows that the main drawback of the QCT approximation is that it does not correctly reproduce the terms \( C_{ij}(0 \rightarrow 2) \). This result is not surprising since these transitions have large rate coefficients when there is a quasi-resonance between the H₂O and H₂ rotational levels, i.e. transitions with \( \Delta \nu > 500 \text{ K} \). At the QCT level, quasi-resonant effects are not included properly owing to the approximate quantization procedure.

3.3. Discussion

In the previous sections, we compared the results of various CRC sets for o–H₂O. The comparisons were made by considering the lines that involve energy levels below the 20th one (i.e. \( E_u < 900 \text{ K} \)). With respect to the water symmetry, calculations were also performed for the p–H₂O molecule and the conclusions were found to be similar; i.e., the quantum thermalised and QCT CRC give qualitatively similar results for the line intensities, when considering both o–H₂ and p–H₂ as collisional partners, with maximum differences for the bulk of the lines of about a factor 3.

With respect to the number of H₂O levels considered, a similar statistical analysis has been performed considering the lines that involve the first 35 energy levels. The differences for the ratios were found to be greater for the lines with \( E_u > 900 \text{ K} \). This qualitatively results in larger variations in the normalised standard deviations (i.e. would magnify the scale of \( \sigma \) in Figs. 2–4). This is illustrated in Fig. 11 where the mean value and standard deviations are given, for the ratio between the o–H₂ STS and QCT CRC. In this figure, we consider all the lines with energy level below the 35th level and for the case of a water abundance \( X(\text{H}_2\text{O}) = 10^{-6} \). The results are to be compared to the results shown in Fig. 4 where only the first 20 levels were considered.

Finally, to a first order, it can be seen that the variations in intensities from one set to the other are linearly correlated to the CRC variations. This is illustrated by considering the critical densities related to the various sets of CRC discussed in the
previous sections, which are reported in Table 1. Comparing, as an example, the critical densities related to the p–H$_2$ QCT and thermalised CRC, we can see that the maximum differences is a factor 3, which is similar to the maximum difference found for the intensity ratio (see Sect. 3.2).

4. The o–H$_2$ / p–H$_2$ dichotomy

At the present time, apart from H$_2$O, only a few collisional systems have been treated that consider both o–H$_2$ and p–H$_2$ as collisional partners (i.e. CO by Wernli et al. (2006); HC$_3$N by Wernli et al. (2007a); SiS by Lique & Klos (2008); Klos & Lique (2008); H$_2$CO by Troscompt et al. (2009); HNC by Dumouchel et al. (2011); CN$^-$ by Klos & Lique (2011); SO$_2$ by Cernicharo et al. (2011); HF by Guillou & Stoecklin (2012); HDO by Faure et al. (2012)). Except in the CN$^-$ case, a common conclusion is that the o–H$_2$ CRC are larger than for p–H$_2$. In the particular case of water, the differences are rather large, with CRC for o–H$_2$ that can be larger by up to a factor ten compared to p–H$_2$. This implies that the population of
Table 1. Critical densities for the lines that involve the first 15 $\rm{o-H_2}$ energy levels, at $T_K = 200$ K.

| transition | $\nu$ (GHz) | He | $\rm{p-H_2}$ | STS | QCT | THER | STS | QCT | THER | STS |
|------------|-------------|----|--------------|-----|-----|------|-----|-----|------|-----|
| $0_{1,0}-5_{2,3}$ | 22.6 | 1.2(3) | 1.1(3) | 3.3(2) | 4.2(2) | 1.1(3) | 2.9(2) | 2.9(2) |
| $1_{0,0}-5_{2,3}$ | 38.0 | 5.2(6) | 2.9(6) | 2.8(6) | 4.6(9) | 1.5(6) | 1.4(6) | 1.4(6) |
| $0_{1,0}-4_{2,3}$ | 448. | 5.9(6) | 3.9(6) | 3.5(6) | 6.1(6) | 1.4(6) | 1.5(6) | 1.5(6) |
| $1_{0,0}-4_{2,3}$ | 557. | 8.1(7) | 4.8(7) | 3.4(7) | 6.9(7) | 3.1(7) | 1.4(7) | 1.4(7) |
| $0_{1,0}-3_{2,3}$ | 1097. | 6.7(8) | 1.4(8) | 2.7(8) | 5.8(8) | 1.1(8) | 1.1(8) | 1.1(8) |
| $1_{0,0}-3_{2,3}$ | 1153. | 2.2(8) | 1.1(8) | 1.1(8) | 2.0(8) | 4.9(7) | 4.3(7) | 4.3(7) |
| $0_{1,0}-2_{2,3}$ | 1163. | 9.1(8) | 1.5(9) | 3.5(8) | 7.2(8) | 7.4(8) | 1.5(8) | 1.5(8) |
| $1_{0,0}-2_{2,3}$ | 114. | 1.6(9) | 1.1(9) | 6.6(8) | 1.6(9) | 4.3(8) | 2.6(8) | 2.6(8) |
| $2_{1,0}-2_{2,3}$ | 1661. | 1.9(9) | 2.6(9) | 9.7(8) | 1.9(9) | 1.4(9) | 4.2(8) | 4.2(8) |
| $2_{1,0}-1_{2,1}$ | 1670. | 1.3(9) | 8.4(8) | 6.6(8) | 1.1(9) | 6.7(8) | 3.3(8) | 3.3(8) |
| $3_{0,0}-5_{2,3}$ | 1714. | 2.2(8) | 2.2(8) | 1.4(8) | 2.0(8) | 2.2(8) | 8.7(8) | 8.7(8) |
| $3_{0,0}-4_{2,3}$ | 1717. | 1.8(9) | 6.3(8) | 8.6(8) | 1.4(9) | 4.6(8) | 4.1(8) | 4.1(8) |
| $2_{1,0}-3_{2,1}$ | 1919. | 1.9(9) | 7.1(8) | 8.0(8) | 1.1(9) | 3.0(8) | 4.8(8) | 4.8(8) |
| $3_{0,0}-3_{2,1}$ | 2196. | 4.6(9) | 2.0(9) | 2.5(9) | 4.0(9) | 1.0(9) | 1.2(9) | 1.2(9) |
| $4_{1,0}-5_{2,3}$ | 2222. | 6.4(9) | 5.9(8) | 3.1(9) | 6.1(9) | 4.2(8) | 1.2(9) | 1.2(9) |
| $4_{1,0}-4_{2,3}$ | 2264. | 7.1(9) | 5.4(9) | 3.3(9) | 5.8(9) | 1.9(9) | 1.5(9) | 1.5(9) |
| $4_{1,0}-3_{2,3}$ | 2463. | 1.0(10) | 3.0(9) | 4.7(9) | 6.9(9) | 2.2(9) | 2.5(9) | 2.5(9) |
| $4_{1,0}-3_{0,0}$ | 2641. | 9.9(9) | 4.2(9) | 4.9(9) | 6.5(9) | 3.0(9) | 3.0(9) | 3.0(9) |
| $5_{1,0}-1_{2,1}$ | 2774. | 1.1(10) | 5.3(9) | 5.0(9) | 7.0(9) | 4.2(9) | 2.8(9) | 2.8(9) |
| $5_{1,0}-3_{2,1}$ | 2971. | 1.6(10) | 1.9(10) | 7.4(9) | 8.8(9) | 7.3(9) | 6.0(9) | 6.0(9) |
| $5_{1,0}-4_{2,3}$ | 3013. | 1.7(10) | 8.3(9) | 8.7(9) | 1.1(10) | 5.5(9) | 6.0(9) | 6.0(9) |
| $5_{1,0}-5_{2,3}$ | 3655. | 3.9(10) | 1.9(10) | 2.0(10) | 2.2(10) | 1.2(10) | 1.5(10) | 1.5(10) |
| $4_{1,0}-4_{2,3}$ | 3807. | 4.6(10) | 3.6(10) | 2.4(10) | 2.9(10) | 2.1(10) | 1.7(10) | 1.7(10) |
| $5_{1,0}-3_{2,3}$ | 3977. | 4.3(10) | 4.4(10) | 2.1(10) | 3.2(10) | 3.9(10) | 1.2(10) | 1.2(10) |
| $5_{1,0}-5_{2,3}$ | 4457. | 1.3(10) | 1.3(10) | 9.7(9) | 1.7(10) | 6.7(9) | 5.3(9) | 5.3(9) |
| $3_{0,0}-2_{2,1}$ | 4512. | 1.0(11) | 4.6(10) | 4.4(10) | 5.7(10) | 3.1(10) | 3.3(10) | 3.3(10) |
| $4_{1,0}-2_{2,1}$ | 5107. | 2.0(11) | 9.7(10) | 8.6(10) | 1.1(11) | 5.5(10) | 7.4(10) | 7.4(10) |
| $5_{1,0}-4_{2,3}$ | 6646. | 4.9(11) | 4.9(11) | 1.3(11) | 3.4(11) | 8.8(10) | 1.2(11) | 1.2(11) |
| $5_{1,0}-5_{2,3}$ | 7368. | 5.1(11) | 5.1(11) | 8.2(10) | 4.8(11) | 8.5(10) | 7.5(10) | 7.6(10) |

Notes. The critical densities are given for the He CRC of Green et al. (1993), the QCT CRC of Faure et al. (2007) and the quantum CRC of Dubernet et al. (2009) and Daniel et al. (2011). In the last case, the values are given for both STS and thermalised CRC.

Fig. 8. Comparison of the results based on the thermalised and STS CRC from Daniel et al. (2011) for o-H$_2$ and for gas temperatures in the range 200–1000 K and for a water abundance $\chi(\text{H}_2\text{O})=10^{-8}$.

The mean value and normalised standard deviation are plotted in Fig. 12, for the three values of the water abundance considered in this work. In this figure, we see that the mean value and normalised standard deviation will depend differently on the protoplanetary disk. This has also been discussed for the H$_2$CO molecule. Troscianek et al. (2009) find that the H$_2$ OTPR was crucial in explaining the excitation of the 1$_{11}$–1$_{10}$ line and that it is possible to accurately constrain the H$_2$ OTPR ratio from its observation. On the other hand, Guzmán et al. (2011) find that for the physical conditions which are typical of the Horsehead nebula, the H$_2$CO lines observed in their study are insensitive to the H$_2$ OTPR. A similar conclusion was obtained by Parise et al. (2011) for the deuterated isotopomers of H$_2$ which were found to be marginally affected by the H$_2$ OTPR for the conditions typical of prestellar cores (see also Pagani et al. 2009).

4.1. State-to-state rate coefficients

The mean value and normalised standard deviation are plotted in Fig. 12, for the three values of the water abundance considered in this work. In this figure, we see that the mean value and normalised standard deviation will depend differently on the...
Fig. 9. Ratio $\frac{I_{\text{THER}}}{I_{\text{QCT}}}$ for a few transitions commonly observed with the Herschel satellite. The thermalised CRC are from Dubernet et al. (2009) and Daniel et al. (2011) and the QCT CRC from Faure et al. (2007). The ratios are given for collisions that involve $o$–H$_2$ (left figure) and $p$–H$_2$ (right figure) in each panel.
Fig. 10. Comparison of the mean (left column) and normalised standard deviation (right column) obtained for the ratios $I/\bar{I}_{\text{approx}}$ and dealing with $p$-H$_2$. The approximation consists in neglecting the terms $C_{j'i'j} (j^2 \rightarrow j^2')$ with $\Delta j^2 \geq 2$ in the calculation of the thermalised CRC. The results obtained with this approximation are compared to the quantum state-to-state CRC (black lines) from Dubernet et al. (2009) and Daniel et al. (2011), the QCT CRC (red lines) from Faure et al. (2007) and thermalised CRC (blue lines) from Dubernet et al. (2009) and Daniel et al. (2011).

Fig. 11. Mean value and normalised standard deviation obtained comparing the quantum CRC from Dubernet et al. (2009) and Daniel et al. (2011) and QCT CRC from Faure et al. (2007), for a water abundance of $\chi(\text{H}_2\text{O}) = 10^{-6}$ cm$^{-3}$. The lines retained in the comparison have an energy below the one of the 35th level of o–H$_2$O.

collisions with o–H$_2$ or p–H$_2$ according to the energy of the upper level involved in the transition. Additionally, there is a correlation between the sensitivity of the transition to the o–H$_2$/p–H$_2$ symmetry with the position of the upper energy level on the $J$-ladder$^5$. Qualitatively, an increase in the energy of the upper level will be accompanied by an increase in both the mean value and normalised standard deviation. For the transitions that involve an upper energy level below 500 K, we find that independently of the water abundance, the mean value is around one and the normalised standard deviation takes low values (below one). Those lines are thus marginally affected by the nature of the collisional partner.

$^5$ As a reminder, H$_2$O is an asymmetric top with quantum numbers denoted as either $J, K_a, K_c$ or $J, K_+, K_-$. A backbone level corresponds to the lower level in energy for a given value of the principal quantum number $J$. This level corresponds to the lowest possible value for the difference $K_a - K_c$.

4.2. Thermalised rate coefficients

In the previous section, on the basis of the quantum STS CRC, it was shown that the H$_2$ OTRP would differentially influence the intensities of the water transitions. In this section, the same analysis is performed using the thermalised quantum CRC, for high gas temperatures ($T_k > 200$ K) and low gas temperatures ($T_k < 100$ K).

4.2.1. High temperature

Figure 13 shows the means and normalised standard deviations for the ratios $P_{\text{ortho}}/P_{\text{para}}$ obtained using the thermalised quantum
To discuss the low-temperature regime, we ran models with free parameters in the range $T_K \in [20 \text{ K}; 100 \text{ K}]$, $n(\text{H}_2) \in [10^5; 2 \times 10^7] \text{ cm}^{-3}$ and $\chi(\text{H}_2\text{O}) \in (10^{-8}; 10^{-6}; 10^{-4})$. The mean values and normalised standard deviations are calculated for each line by considering all the models of the grid. In Table 2, we give the mean values and standard deviations for all the lines. From this table, it appears that all the lines that are considered are affected by the H$_2$ OTPR. The main effect, as discussed earlier, is to obtain an increase in intensity when considering o–H$_2$ as a collisional partner for the transitions with upper energy level below 500 K. On the other hand, for the levels with an upper energy level above 500 K, considering p–H$_2$ as a collisional partner results in higher intensities. Additionally, the line intensities are affected differentially by the symmetry of the collisional partner. This differential effect is presented in Fig. 14 where the intensity difference is induced by the increase in magnitude of the CRC with energy level above 500 K, considering p–H$_2$ as a collisional partner for the transitions with upper energy level below 500 K. On the other hand, for the levels with an upper energy level above 500 K, considering o–H$_2$ as a collisional partner results in higher intensities. Additionally, the line intensities are affected differentially by the symmetry of the collisional partner. This differential effect is presented in Fig. 14 where the intensity

Table 2. Mean values and normalised standard deviations for the ratios $I_{\text{ortho}}/I_{\text{trans}}$ obtained with the thermalised CRC from Dubernet et al. (2009) and Daniel et al. (2011), with parameters in the range $20 < T_K < 100$ K and $10^5 < n(\text{H}_2) < 2 \times 10^7$ cm$^{-3}$.

| transition | $\nu$ (GHz) | $\lambda$ (\mu m) | $E_n$ (K) | $\chi(\text{H}_2\text{O}) = 10^{-8}$ | $\chi(\text{H}_2\text{O}) = 10^{-6}$ | $\chi(\text{H}_2\text{O}) = 10^{-4}$ |
|------------|-------------|-------------------|----------|----------------------------------|----------------------------------|----------------------------------|
| $1_{10}-1_{01}$ | 557. | 538. | 61. | 2.8 | 0.8 | 1.4 | 0.4 | 1.3 | 0.3 |
| $3_{12}-3_{03}$ | 1097. | 273. | 249. | 3.2 | 0.7 | 2.7 | 0.8 | 2.3 | 1.1 |
| $3_{12}-3_{12}$ | 1163. | 258. | 305. | 2.8 | 0.7 | 2.6 | 0.8 | 2.1 | 0.8 |
| $2_{21}-2_{12}$ | 1661. | 180. | 194. | 2.5 | 0.6 | 2.1 | 0.6 | 1.5 | 0.3 |
| $2_{12}-1_{01}$ | 1670. | 180. | 114. | 2.1 | 0.6 | 1.7 | 0.5 | 1.6 | 0.5 |
| $3_{03}-3_{12}$ | 1717. | 175. | 197. | 2.2 | 0.5 | 2.0 | 0.7 | 1.2 | 0.4 |
| $3_{03}-3_{03}$ | 2196. | 136. | 411. | 2.6 | 0.7 | 2.0 | 0.6 | 1.8 | 0.6 |
| $4_{32}-4_{14}$ | 2264. | 132. | 432. | 2.9 | 0.6 | 2.3 | 0.8 | 2.0 | 0.8 |
| $4_{14}-3_{03}$ | 2640. | 114. | 323. | 1.8 | 0.4 | 1.7 | 0.6 | 1.5 | 0.4 |
| $2_{21}-1_{10}$ | 2774. | 108. | 194. | 2.5 | 0.7 | 2.5 | 0.9 | 2.0 | 0.5 |
| $5_{14}-4_{23}$ | 2971. | 101. | 575. | 1.9 | 0.4 | 1.6 | 0.4 | 1.3 | 0.6 |
| $5_{05}-4_{14}$ | 3013. | 99. | 468. | 1.7 | 0.3 | 1.6 | 0.5 | 1.6 | 0.6 |
| $6_{16}-5_{05}$ | 3655. | 82. | 644. | 1.1 | 0.2 | 1.1 | 0.2 | 1.1 | 0.3 |
| $4_{23}-3_{12}$ | 3807. | 79. | 432. | 2.4 | 0.4 | 2.0 | 0.7 | 1.8 | 0.6 |
| $3_{21}-2_{12}$ | 3977. | 75. | 305. | 3.2 | 0.8 | 3.4 | 1.6 | 2.4 | 1.1 |
| $7_{07}-6_{16}$ | 4167. | 72. | 843. | 0.5 | 0.2 | 0.7 | 0.2 | 0.8 | 0.1 |
| $3_{10}-3_{03}$ | 4457. | 67. | 411. | 2.6 | 0.5 | 2.5 | 0.8 | 2.3 | 0.7 |
| $6_{25}-5_{14}$ | 4512. | 66. | 411. | 2.4 | 0.4 | 2.1 | 0.7 | 1.9 | 0.6 |
| $4_{12}-3_{21}$ | 4600. | 65. | 796. | 0.8 | 0.2 | 1.0 | 0.3 | 1.0 | 0.3 |
| $4_{41}-3_{30}$ | 5107. | 59. | 550. | 1.2 | 0.4 | 1.3 | 0.3 | 1.0 | 0.3 |
| $5_{12}-4_{23}$ | 6076. | 49. | 702. | 0.5 | 0.4 | 0.7 | 0.3 | 0.7 | 0.4 |
| $5_{23}-4_{14}$ | 6249. | 48. | 732. | 0.5 | 0.6 | 0.8 | 0.3 | 0.8 | 0.3 |
| $5_{12}-4_{14}$ | 6646. | 45. | 642. | 0.9 | 0.4 | 1.1 | 0.3 | 1.0 | 0.4 |
| $4_{32}-3_{03}$ | 7368. | 41. | 550. | 1.7 | 0.2 | 1.5 | 0.4 | 1.3 | 0.2 |

![Fig. 13](image1.png) Same as Fig. 12 but considering the quantum thermalized CRC from Dubernet et al. (2009) and Daniel et al. (2011).
ratios are shown for some of the lines that involve the lowest energy levels of $\text{o–H}_2\text{O}$. From this figure it can be seen that under specific physical conditions, the intensity ratio can take high values for certain lines (i.e. larger than 15, like for example for the $2_{21}-2_{12}$) while it remains low for other lines (i.e. below 2, like for example for the $4_{14}-3_{03}$). Since, the lines depend differentially on the H$_2$ OTPR, it is in principle possible to determine the H$_2$ OTPR for the molecules of the gas from an accurate modelling of the water line intensities observations. In practice, however, this can be a difficult task due to the dependence of the line intensities on other parameters of the model, such as the gas temperature, H$_2$ volume density, and geometry of the source. Moreover, this is only feasible if it relies on a large set of observations. This puts strong limits on the usefulness of water for deriving the H$_2$ OTPR at low temperature ($T_K < 50$ K) since only a few transitions will be observable with reasonable sensitivity (i.e. with RMS < 10 mK).

5. Dust radiative pumping

All the comparisons performed in Sects. 2 and 3 ignored the possibility of pumping by IR and submillimetre dust radiation. This
would correspond to an extreme case, not physically relevant to all astrophysical objects. Indeed, as an example, radiative pumping by continuum photons plays an important role in the H$_2$O excitation in AGB circumstellar envelopes. In short, considering this additional mechanism in the population of the water energy levels would reduce the differences between line intensities obtained from differencing CRC. This is illustrated in Fig. 15, where we consider the $F_{\text{ortho}}/F_{\text{para}}$ ratios obtained from the STS CRC. In this case, we chose to compare the results based on these CRC since we found in Sect. 4 that the respective intensities show large differences, thereby emphasizing the role played by dust radiation. The model parameters are $n$(H$_2$) = 10$^6$ cm$^{-3}$, $T_K$ = 200 K, and $\chi$(H$_2$O) = 10$^{-8}$. In the model, we assume a gas-to-dust mass ratio of 100, and the dust composition corresponds to a mixture of astrophysical silicates and amorphous carbon grains, with opacities taken from Draine & Lee (1984).

In the modelling, we varied the dust temperature ($T_D$) from 5 K to 200 K. Moreover, to compute $I$, we assume $T_B$ = $T_D$ for the background temperature. From this figure, we see that, while the mean values and standard deviations are high at low dust temperatures ($m \sim 7$ and $\sigma \sim 5$), they are considerably reduced when $T_D$ increases. For dust temperatures above 50 K, we obtain $m \sim 1$ and $\sigma < 0.2$, which implies that the influence of differencing CRC starts to be minimal since the population of the H$_2$O energy levels is dominated by radiative pumping and no longer by the collisions.

**6. Conclusions**

We performed non-local non-LTE excitation and radiative transfer calculations aiming at comparing the line intensities predicted for water vapour when making use of differencing CRC sets. The CRC sets compared are the He quantum rate coefficients (Green et al. 1993), H$_2$ quantum rate coefficients of (Dubernet et al. 2006, 2009; Daniel et al. 2010, 2011), and H$_2$ quasi-classical rate coefficients (Faure et al. 2007). The comparison was performed at relatively high temperature (200 K < $T_K$ < 1000 K) and an emphasis was made on the comparison of the H$_2$ CRC sets, since the quantum rate coefficients have only lately become available and many recent astrophysical studies have made use of the QCT calculations. In the absence of radiative pumping by dust photons, it was found that the results based on the quantum and QCT rate coefficients sets will lead to line intensities that qualitatively agree, i.e. which are of the same order of magnitude, for the parameter space considered in this work. However, the H$_2$O line emission can differ by a factor of ~3, in the regime of low water abundance ($\chi$(H$_2$O) < 10$^{-8}$) and moderate H$_2$ volume densities ($n$(H$_2$) < 10$^6$ cm$^{-3}$).

These differences should not drastically affect the conclusions obtained from modelling the water excitation in astrophysical objects, but the water vapour abundance derived on the basis of the QCT rate coefficients will differ with the one derived from the quantum rate coefficients, with differences still up to a factor of ~3. We note, however, that such differences will be attenuated by the presence of a dust continuum source of radiation. Additionally, masing lines are not considered in the present analysis. A similar comparison for the case of masing lines is presented in Daniel & Cernicharo (2012), where the impact induced by the CRC on the lines that will be observable with ALMA is discussed. Finally, we emphasise that the impact of the various CRC sets is discussed on the basis of statistics over the most intense lines. The current results can thus be affected to some extent by the choice of the subset of lines used in the analysis.

The differences found between the QCT and quantum CRC can give clues to the uncertainty introduced in the modelling owing to the uncertainties on the rate coefficients. Indeed, as discussed in Dubernet et al. (2009) and Daniel et al. (2010), the QCT and quantum CRC typically agree within a factor of 3 for the highest rate coefficients. In the current study, we obtain the same factor between the line intensities obtained with two sets. Therefore, in a first approximation, the error on the rate coefficients will translate similarly to line intensities. Recently, Yang et al. (2011) find a good agreement between experimental integral cross sections and quantum calculations, showing the good accuracy of the PES on which the quantum calculations are based. Depending on the energy of the level considered and the gas temperature, it was said in Dubernet et al. (2009) and Daniel et al. (2010) that the accuracy of the quantum CRC will range from a few to a few ten percentage points and such errors should scale linearly on line intensities.

We performed additional test calculations with an ad hoc set of thermalised CRC in which the STS rate coefficients associated to the H$_2$ transitions with $\Delta j_2 \neq 0$ were removed. The comparison of the results obtained with this ad hoc set and the QCT rate coefficients showed particularly good agreement. Over the temperature range $T =$ 200–1000 K, the intensities predicted with those two sets agree within 30%. It is concluded that the main drawback of the QCT approximation is that it does not correctly reproduce the terms $C_3(0 \rightarrow 2)$.

By considering the quantum STS and quantum thermalised CRC, it was found that line intensities will be largely affected by considering the first excited state, in the case of p–H$_2$. The differences start to be non-negligible (i.e. greater than 20%) for temperatures higher than $T_K$ ~ 60 K, reaching a maximum of a factor ~3 around 200 K. On the other hand, the intensities predicted with the STS and thermalised CRC are similar for the collisions that involve o–H$_2$. Such behaviour can be extrapolated to other molecules that show strong differences for the collisions between o–H$_2$ and p–H$_2$. Indeed, these differences arise because of the interaction with the quadrupole of H$_2$, and significant differences for the CRC with p–H$_2$ or o–H$_2$ imply that the STS rate coefficients for p–H$_2$ in $j_2 = 0$ or $j_2 = 2$ will show large differences, too. Therefore, the use of STS rather than thermalised CRC for such molecules will lead to overestimating of the molecular abundances for temperatures higher than $T_K$ ~ 60 K.
By comparing the line intensities obtained using either o–H$_2$ or p–H$_2$ as a collisional partner, we found that under particular physical conditions ($n$(H$_2$) and $T_K$), the water lines will be differentially affected by the symmetry of the H$_2$ molecule. This effect is obtained when the gas temperature is low, i.e. $T_K < 100$ K. In contrast, at high temperature, the lines become insensitive to the H$_2$ symmetry. Since some transitions will show large intensity variations with respect to the H$_2$ symmetry, the modelling of the water excitation may provide a means to derive the H$_2$ OTPR. The lines to be considered in such an estimate will, however, depend on the physical conditions prevailing in the object under study, so it is necessary to perform a case-by-case modelling.

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References
Cernicharo, J., & Crovisier, J. 2005, Space Sci. Rev., 119, 29
Cernicharo, J., Thum, C., Hein, H., et al. 1990, A&A, 231, L15
Cernicharo, J., González-Alfonso, E., Alcolea, J., Bachiller, R., & John, D. 1994, ApJ, 432, L59
Cernicharo, J., González-Alfonso, E., & Bachiller, R. 1996, A&A, 305
Cernicharo, J., Pardo, E., Serabyn, E., et al. 1999, ApJ, 520, L131
Cernicharo, J., Goicoechea, J. R., Daniel, F., et al. 2006a, ApJ, 649, L33
Cernicharo, J., Goicoechea, J. R., Pardo, J. R., & Asensio-Ramos, A. 2006b, ApJ, 642, 940
Cernicharo, J., Ceccarelli, C., Ménard, F., Pinte, C., & Fuente, A. 2009, ApJ, 703, L123
Cernicharo, J., Spiegel, A., Balañá, C., et al. 2011, A&A, 531, A103
Cheung, A. C., Rank, D. M., Townes, C. H., Thornton, D. D., & Welch, W. J. 1969, Nature, 221, 626
Daniel, F., & Cernicharo, J. 2008, A&A, 488, 1237
Daniel, F., & Cernicharo, J. 2012, A&A, submitted
Daniel, F., Dubernet, M.-L., Pacaud, F., & Grosjean, A. 2010, A&A, 517, A15
Daniel, F., Dubernet, M.-L., & Grosjean, A. 2011, A&A, 536, A76
Draine, B. T., & Lee, H. M. 1984, ApJ, 285, 89
Dubernet, M.-L., & Grosjean, A. 2002, A&A, 390, 793
Dubernet, M.-L., Daniel, F., Grosjean, A., et al. 2006, A&A, 460, 323
Dubernet, M.-L., Daniel, F., Grosjean, A., & Lin, C. Y. 2009, A&A, 497, 911
Dumouchel, F., Klos, J., & Lique, F. 2011, Phys. Chem. Chem. Phys., 13, 8204
Faure, A., & Josselin, E. 2008, A&A, 492, 257
Faure, A., Valiron, P., Wernli, M., et al. 2005, J. Chem. Phys., 122, 221102
Faure, A., Crimier, N., Ceccarelli, C., et al. 2007, A&A, 472, 1029
Faure, A., Wiesenfeld, L., Scribano, Y., & Ceccarelli, C. 2012, MNRAS, 420, 699
González-Alfonso, E., Cernicharo, J., Banett, R., et al. 2012, A&A, in press, DOI: 10.1051/0004-6361/201219912
Hogerheijde, M. R., Bergin, E. A., Brinch, C., et al. 2011, Science, 334, 338
Kessler, M. F., Steinz, J. A., Anderegg, M. E., et al. 1996, A&A, 315, L27
Klos, J., & Lique, F. 2008, MNRAS, 390, 239
Klos, J., & Lique, F. 2011, MNRAS, 418, 271
Kristensen, L. E., van Dishoeck, E. F., Bergin, E. A., et al. 2012, A&A, 542, A8
Lique, F., & Klos, J. 2008, J. Chem. Phys., 128, 034306
Lis, D. C., Phillips, T. G., Goldsmith, P. F., et al. 2010, A&A, 521, L26
Melnick, G. J., Stauffer, J. R., Ashby, M. L. N., et al. 2000, ApJ, 539, L77
Menten, K., & Melnick, G. J. 1991, ApJ, 377, 647
Menten, K. M., Melnick, G. J., Phillips, T. G., & Neufeld, D. A. 1990a, ApJ, 363, L27
Menten, K. M., Melnick, G. J., & Phillips, T. G. 1990b, ApJ, 350, L41
Neufeld, D. A., & Kaufman, M. J. 1993, ApJ, 418, 263
Neufeld, D. A., Lepp, S., & Melnick, G. J. 1995, ApJ, 100, 132
Neufeld, D. A., Gonzalez-Alfonso, E., Melnick, G. J., et al. 2011, ApJ, 727, L29
North, H. L., von Schéele, F., Frisk, U., et al. 2003, A&A, 402, L21
Puglisi, L., Vastel, C., Hugo, E., et al. 2009, A&A, 494, 623
Purise, B., Belloche, A., Du, F., Güsten, R., & Menten, K. M. 2011, A&A, 526, A3
Phillips, T. G., Kwan, J., & Huggins, P. J. 1980, in IAU Symp. 87, ed. B. H. Andrew (Dordrecht: Reidel), 21
Phillips, T. R., Maluendes, S., McLean, A. D., & Green, S. 1994, J. Chem. Phys., 101, 5824
Phillips, T. R., Maluendes, S., & Green, S. 1996, J. Phys. Chem., 107, 467
Phillips, T. R., Ridgler, J. R., Passvogel, T., et al. 2010, A&A, 518, L1
Rothman, L. S., Gordon, I. E., Barbe, A., et al. 2009, J. Quant. Spec. Radiat., 110, 533
Royer, P., Decin, L., Wesson, R., Barlow, M. J., et al. 2010, A&A, 518, L145
Troscompt, N., Faure, A., Wiesenfeld, L., Ceccarelli, C., & Valiron, P. 2009, A&A, 493, 687
Troscompt, N., Faure, A., Maret, S., et al. 2009, A&A, 506, 1243
Valiron, P., Wernli, M., Faure, A., et al. 2008, J. Chem. Phys., 129, 134306
Watson, D. M., Bohac, C. J., Hull, C., et al. 2007, Nature, 448, 1026
Wernli, M., Valiron, P., Faure, A., et al. 2006, A&A, 446, 367
Wernli, M., Wiesenfeld, L., Faure, A., & Valiron, P. 2007b, A&A, 475, 391
Yang, C.-H., Sarma, G., Parker, D. H., Ter Meulen, J. J., & Wiesenfeld, L. 2011, J. Chem. Phys., 134, 204308