Role of Magnetic Fields in the Formation of Direct Collapse Black Holes

Muhammad A. Latif1, Dominik R. G. Schleicher2, and Sadegh Khochfar3

1 Physics Department, College of Science, United Arab Emirates University, PO Box 15551, Al-Ain, UAE; latifine@gmail.com
2 Astronomy Department, Universidad de Concepción, Barrio Universitario, Concepción, Chile
3 Institute for Astronomy, University of Edinburgh, Royal Observatory, Blackford Hill, Edinburgh EH9 3HJ, UK

Received 2022 October 7; revised 2023 February 3; accepted 2023 February 15; published 2023 March 15

Abstract

Direct collapse black holes are the leading candidates for the origin of the first supermassive black holes. However, the role of magnetic fields during their formation is still unclear as none of the previous studies has been evolved long enough to assess their impact during the accretion phase. Here, we report the results from a suite of 3D cosmological magnetohydrodynamic (MHD) simulations which are evolved for 1.6 Myr comparable to the expected lifetime of supermassive stars (SMSs). Our findings suggest that magnetic fields are rapidly amplified by strong accretion shocks irrespective of the initial magnetic field strength and reach the saturation state. They stabilize the accretion disks and significantly reduce fragmentation by enhancing the Jeans mass in comparison with pure hydrodynamical runs. Although the initial clump masses are larger in MHD runs, the rapid coalescence of clumps in non-MHD cases due to the higher degree of fragmentation results in similar masses. Overall, the central clumps have masses of $10^5 M_\odot$ and the mean mass accretion rates of $\sim 0.1 M_\odot$ yr$^{-1}$ are similar in both MHD and non-MHD cases. The multiplicity of SMSs is significantly reduced in MHD simulations. Such strongly amplified magnetic fields are expected to launch jets and outflows which may be detected with upcoming radio telescopes.

Unified Astronomy Thesaurus concepts: Population III stars (1285); Early universe (435); Supermassive black holes (1663); Computational methods (1965); Primordial galaxies (1293)

1. Introduction

High-redshift surveys have detected more than 400 quasars at $z > 5.7$ (Fan et al. 2003; Mortlock et al. 2011; Wu et al. 2015; Bañados et al. 2018; Wang et al. 2021) powered by supermassive black holes (SMBHs) of about $\sim 10^9 M_\odot$. The existence of such objects within the first billion years of the universe is still a mystery and poses the biggest challenge to our understanding of early structure formation. Various pathways have been proposed for the formation of black holes, which from the astrophysical point of view can be categorized into three mechanisms: (1) remnants of Population III stars, so-called stellar mass black holes; (2) stellar dynamical processes in dense stellar clusters leading to the formation of a massive black hole; (3) monolithic collapse of a massive protogalactic gas cloud into an intermediate mass black hole, commonly known as the direct collapse black hole (DCBH) scenario. Details of these mechanisms can be found in dedicated reviews (Latif & Ferrara 2016; Woods et al. 2019; Inayoshi et al. 2020). Black holes forming from the core collapse of massive Population III stars at $z \sim 30$ are expected to have about $\sim 100 M_\odot$ (Sugimura et al. 2020; Latif et al. 2022a) and are difficult to grow due to the shallow dark matter potentials of their host halos (Johnson & Bromm 2007; Alvarez et al. 2009; Riaz et al. 2018; Latif & Khochfar 2020). They may require multiple episodes of super-Eddington accretion to reach the observed masses within the first billion years (Lupi et al. 2014; Mayer et al. 2015; Pacucci et al. 2015; Mayer & Bonoli 2019). Runaway stellar collisions during the core collapse of dense stellar clusters may result in a very massive star which subsequently collapses into a black hole of a few times $10^3$–$10^4 M_\odot$ (Devecchi et al. 2012; Katz et al. 2015; Latif et al. 2016a; Yajima & Khochfar 2016; Sakurai et al. 2017; Reinoso et al. 2018; Chon & Omukai 2020; Das et al. 2021; Vergara et al. 2021; see Schleicher et al. 2022 for more details).

The direct collapse scenario yields black holes of $10^5 M_\odot$, which are about two orders of magnitude more massive than in the other scenarios (Latif et al. 2013a; Sakurai et al. 2016). The key requirement for the DCBH mechanism is a mass inflow rate of $\sim 0.1 M_\odot$ yr$^{-1}$ (Hosokawa et al. 2013; Schleicher et al. 2013). Such high accretion rates can be more easily obtained thermodynamically in massive primordial halos by quenching H$_2$ formation which results in an isothermal collapse with $T \sim 8000$ K and larger sound speeds ($\dot{M} \sim c_s^3 / G \sim 0.1 M_\odot$ yr$^{-1} (T / 8000$ K)$^{1/2}$). Alternatively, inflow rates of $\sim 0.1 M_\odot$ yr$^{-1}$ can be obtained dynamically via bars within bars instabilities (Begelman et al. 2006) or through the rapid growth of halos via major mergers in combination with moderate UV flux in metal-free halos (Latif & Volonteri 2015; Wise et al. 2019), or through large baryonic streaming motions (Hirano et al. 2017). Recently, Latif et al. (2022b) found that dense cold turbulent flows give birth to DCBHs without the need of an external UV flux. Numerical simulations investigating the feasibility of the DCBH mechanism find that large accretion rates of $0.1$–$1 M_\odot$ yr$^{-1}$ can be obtained (Latif et al. 2013c, Latif et al. 2020; Regan et al. 2019). However, their number density is still an open question due to the dependence of the required critical UV flux (for suppressing H$_2$ formation) on local conditions and on the environment (Sugimura et al. 2014; Agarwal et al. 2016; Latif et al. 2015).

Previous works mainly focused on hydrodynamical (HD) aspects of the DCBH scenario, and the role of magnetic fields is not yet fully clear. They are expected to influence DCBH formation by transferring angular momentum, exerting...
magnetic torques, and may even suppress fragmentation by enhancing the Jeans mass. Magnetic fields observed in the local universe are thought to be responsible for various astrophysical phenomena including the launch of magnetic outflows and jets (Beck et al. 1999; Beck 2007; Pudritz et al. 2012). Furthermore, observation of rotation measures in high-z quasars up to $z \sim 5.3$ reveal the presence of magnetic fields at earlier times (Murphy 2009; Hammond et al. 2012). Future radio observatories such as ngVLA and SKA will probe magnetic fields at high redshifts (Arshakian et al. 2009; Nyland et al. 2018) which are expected to efficiently form via mechanisms such as the small-scale dynamo (Schleicher & Beck 2013; Schober et al. 2013).

The standard model does not yield any constraints on the strength of the initial magnetic fields. They can be generated through electro-weak or quantum chromodynamics phase transitions during the cosmic inflation or alternatively via mechanisms such as the Biermann battery effect and the transitions during the cosmic inflation (see the review by Widrow et al. 2012). Irrespective of their origin, the seed magnetic fields are many orders of magnitude smaller than the present-day fields. They can be initially strengthened via gravitational compression in the domain of flux freezing and later can get further amplified via the small-scale dynamo as it converts turbulent into magnetic energy on short timescales. In the context of star formation various studies confirm that the small-scale dynamo becomes operational and amplifies seed fields on very short timescales (Schleicher et al. 2010; Sur et al. 2010; Federrath et al. 2011; Schober et al. 2012; Turk et al. 2012; Grete et al. 2019, hereafter G19; Sharda et al. 2020). These studies further suggest that such strong fields may impact the initial mass function of primordial stars. On the other hand, the role of magnetic fields in the formation of DCBHs is not fully clear. Latif et al. (2013b; hereafter L13) and Grete et al. (2019) performed cosmological magnetohydrodynamical (MHD) simulations and have shown that magnetic fields get amplified very efficiently in atomic cooling halos where gas mainly cools by atomic line radiation. Furthermore, Latif et al. (2014; hereafter L14) found that irrespective of the initial seed field strength, the magnetic field is amplified within the freefall timescale in the presence of strong accretion shocks. However, these simulations could not be evolved long enough to determine the role of such magnetic fields during the late accretion phase of supermassive stars (SMSs) due to the exorbitant computational costs.

Recently, Hirano et al. (2021) performed idealized simulations to study the collapse of atomically cooling magnetized gas cloud. They found that magnetic fields enhance the mass accretion onto the gas cloud which results in a higher degree of fragmentation but simultaneously the coalescence rate of clumps gets increased. Consequently, the massive star grows at a faster rate and thus magnetic fields support DCBH formation. However, their simulations were performed for an isolated gas cloud assuming a Bonner–Ebbott sphere and were evolved only for 700 yr. Therefore, it is unclear how magnetic fields regulate the formation of SMSs over longer times in realistic cosmological environments, what is their impact on degree of fragmentation, and how they influence the final masses of the resulting objects. To investigate these questions, we perform 3D MHD cosmological simulations for three distinct halos and evolve them for about 1.6 Myr and compare our results with HD simulations. These simulations enable us to investigate the role of the magnetic fields during the accretion phase.

Our paper is organized as follows. In Section 2, we discuss the numerical methods and the simulation setup. We present our main findings in Section 3 and give our conclusions in Section 4.

### 2. Methods

Numerical simulations are conducted with the cosmological MHD open source code ENZO (Bryan et al. 2014) which utilizes an adaptive mesh refinement approach to cover a large range of spatial scales: from Mpc to AU scales. Enzo employs the Harten–Lax–van Leer Riemann solver with a piecewise linear construction for MHD, the N-body particle-mesh technique to compute dark matter (DM) dynamics and a multigrid Poisson solver for self-gravity calculations. It uses the Dedner scheme (Wang et al. 2008, 2010) for divergence cleaning.

Our simulations start at $z = 150$ with cosmological initial conditions generated from Gaussian random density perturbations with MUSIC (Hahn & Abel 2011) and use the following cosmological parameters from the Planck mission: $\Omega_m = 0.3089$, $\Omega_{\Lambda} = 0.691$, $\Omega_b = 0.0486$, $h = 0.677$, $\sigma_8 = 0.816$, and $n = 0.967$ (Planck Collaboration et al. 2016). We take a comoving periodic box of 1 Mpc h$^{-1}$ in size with top grid resolution of 256$^3$ and the same number of DM particles. The most massive halo of a few times $10^7 M_\odot$ in the computational volume is selected at the earliest redshift of its formation. The selected halo is placed at the center of the box and two additional static grids are added in the central 250 ckpc region yielding an effective DM resolution of $\sim 67 M_\odot$. We further employ up to 15 levels of refinement during the course of the simulation which result in an effective spatial resolution of $\sim 2000$ AU. The same procedure is adopted for all three halos selected from different random seeds. The masses and collapse redshifts of simulated halos are listed in Table 1. A Jeans resolution of at least 64 cells is ensured during the entire course of simulations, which is found to be sufficient to resolve turbulent eddies in cosmological simulations (Federrath et al. 2011; Latif et al. 2013a) for which the small-scale dynamo gets excited to exponentially amplify magnetic fields (L13, L14).

Our refinement criteria are based on the baryonic overdensity, the DM mass resolution, and the Jeans refinement; for details see Latif & Khochfar (2019, 2020). We smooth DM particles at level 10 which corresponds to the physical scale of 0.1 pc. At
and below this scale self-gravity from the baryons dominates in the center of the halos and the smoothing of DM particles avoids a spurious heating of the baryons.

In the presence of radiative cooling, objects can collapse to very high densities for which the Jeans length cannot be resolved due to the limited resolution and as a result they may undergo artificial fragmentation. To further evolve the simulations beyond the initial collapse, a minimum pressure is applied to the cells at the maximum refinement level to prevent them from collapsing further and to make them Jeans stable; see Machacek et al. (2001). Artificial pressure is added to the cells at the maximum refinement level taken to be the maximum of $KG\mu_0^2\Delta_0^2/\mu$ and the thermal pressure where $K$ is chosen to be 100, $\rho_b$ is the gas density, $\Delta_0$ is the cell width at the maximum level, and $\mu$ is the mean particle mass. Doing so may suppress fragmentation over a scale of a few times the cell size at the maximum refinement level which corresponds to a few times 0.01 pc. Using this technique the Jeans length to cell size ratio is 10. Such an approach has been compared to the sink particles method and was shown to yield similar results (Latif et al. 2013c, 2022b).

In our simulations, we employ the non-equilibrium primordial gas chemistry network based on Abel et al. (1997) and Anninos et al. (1997), to evolve six primordial species ($H$, $H^+$, He, He$^+$, He$^{++}$, and e$^-$). We assume here that the halos are illuminated by an intense Lyman–Werner radiation emitted by nearby sources (Agarwal et al. 2016, 2019) which suppresses the formation of H$_2$, leading to an isothermal collapse. This enables us to study the impact of magnetic fields on the formation of DCBHs under isothermal conditions. Our chemical solver is coupled with hydrodynamics and we include cooling from collisional ionization and excitation of H and He, radiative recombination, inverse Compton scattering, and bremsstrahlung radiation.

To identify clumps in our simulations, we employ the clump finder that is publicly available in the YT analysis tool (Turk et al. 2011) where the clump finding algorithm is based on Smith et al. (2009). It works by finding topologically connected sets of cells in the spherical region of a given radius. A clump is defined as the mass contained between a local density maximum and the lowest isodensity surface surrounding it. A clump contains at least 20 cells and is considered gravitationally bound if its gravitational energy exceeds both the thermal and kinetic energies locally. The algorithm works in density space; the first contour spans the entire range of density within the sphere, effectively creating one large contour which becomes the parent clump of all others to be found later. In the second iteration, contours are created with the same maximum but with the minimum density increased by 1/4 dex. If more than one contour is found then such a group of cells becomes a child clump. This process continues in a recursive manner until the minimum density reaches the maximum one. Effectively, this creates a family tree of clumps and only gravitationally bound child clumps are considered unless no child is found. We take a sphere of radius 10 pc centered at the point of maximum density and set the minimum density to be $10^{-16}$ g cm$^{-3}$. We also experimented with further decreasing the minimum density to $10^{-17}$ g cm$^{-3}$, increasing the size of the sphere up to 15 pc, and increasing the minimum number of cells to 32 in the clump, and found similar results.

3. Results

We performed cosmological MHD simulations for three distinct halos of a few times $10^7 M_\odot$ and compared our results with HD runs. For the MHD simulations, we took the fiducial value of the initial seed magnetic field to be $10^{-14}$ G at an initial redshift of 150. This choice of the field is motivated by our previous works L13 and L14. In fact, we found in L14 and G19 that, irrespective of the initial field strength, the magnetic field reaches an equipartition value in the presence of strong accretion shocks during the collapse. We also investigated a case with an initial magnetic field strength of $10^{-20}$ G. In total, we performed seven simulations with and without magnetic fields and present their findings here.

Gas falls into the DM potentials, gets heated due to the virialization shocks and thereafter atomic line cooling kicks in, which leads to an isothermal collapse with $T \sim 8000$ K in the absence of molecular hydrogen. Consequently, a monolithic collapse occurs and the gas densities in the halo center reach $10^{10}$ cm$^{-3}$ at scales of about 2000 AU as shown in Figure 1. The density profiles follow approximately an $R^{-2}$ behavior as expected under isothermal conditions and the bumps on the profiles reveal the presence of additional clumps at these radii. Moreover, these bumps are more frequent in non-MHD runs due to the higher degree of fragmentation, the implications of which we discuss below. Overall, about a few times $10^8 M_\odot$ of gas lies in all simulated halos and small differences in the enclosed gas mass below 10 pc scales are due to fragmentation.

3.1. Magnetic Field Amplification

Magnetic fields get amplified during the gravitational collapse up to 1 G in the center of the halos as shown in Figure 1. Initially, the strength of the magnetic field rises slowly but between 20 and 40 pc it increases by many orders of magnitudes up to $10^{-3}$ G and then continues to increase toward the halo center. We observe here that the magnetic field strength increases by 14 orders of magnitude (even 20 for an initially weak field), while the density increases by 10 orders of magnitude during collapse. This is significantly beyond the amplification expected from compression, where $B \sim \rho^{2/3}$ under flux freezing. Any additional contribution is a consequence of rapid amplification by strong accretion shocks and the small-scale dynamo as found in L13, L14, and G19.

To understand the rapid amplification of the magnetic fields, we show the magnetic energy divided by the maximum possible contribution from flux freezing ($\rho^{1/3}$) in Figure 2 assuming a spherical collapse. The ratio of magnetic energy to $\rho^{1/3}$ shows a big jump between 10 and 40 pc for all halos and irrespective of the initial magnetic field strength. The magnetic field growth time ($1/\omega$) is about 1000 yr, which is about an order of magnitude smaller than the collapse timescale. We attribute this rapid amplification of magnetic fields to the strong accretion shocks occurring at these radii which significantly reduce the amplification timescale and result in a swift amplification of the magnetic fields. Such rapid amplification was investigated in detail by L14 who showed a correlation between the strength of the accretion shocks and rapid amplification; see Section 3.1 of L14 and discussion therein. More recent works by Hirano et al. (2021) and Hirano & Machida (2022) show similarly swift amplification. Initially the amplification occurs at the edge of the accretion disk and subsequently grows with time. By the end of the simulations
the magnetic field strength spreads outwards up to 30 pc and becomes almost constant in the center.

To assess the saturation of magnetic fields, we plot the ratio of magnetic to turbulent energy in Figure 2.

\[ E_B / E_{\text{turb}} = \frac{B^2}{\rho v_{\text{turb}}^2} \]

where \( B \) is the magnetic field strength, \( \rho \) is the density, and \( v_{\text{turb}} \) is the turbulent velocity. The ratio of turbulent to magnetic energy is almost constant at larger radii, rapidly increases during strong accretion shocks, and reaches close to unity. This suggests that the magnetic field strength spreads outwards up to 30 pc and becomes almost constant in the center.

To assess the saturation of magnetic fields, we plot the ratio of magnetic to turbulent energy in Figure 2. We estimate the turbulent energy as \( E_{\text{turb}} = 0.5 \rho v_{\text{turb}}^2 \) and

\[ v_{\text{turb}} = \sqrt{v_{\text{rms}}^2 - v_{\text{rot}}^2 - v_{\text{rad}}^2} \]

where \( v_{\text{rms}} \) is the root mean square velocity, \( v_{\text{rot}} \) is the rotational velocity, and \( v_{\text{rad}} \) is the radial infall velocity. The ratio of turbulent to magnetic energy is almost constant at larger radii, rapidly increases during strong accretion shocks, and reaches close to unity. This suggests that
the magnetic energy is in equipartition with the turbulent energy and the magnetic field is saturated. In Figure 3, we show the time evolution of the magnetic fields strength in all halos along with the case of the initial magnetic field strength of $10^{-20}$ G. It is found that the amplification of the magnetic fields starts in the center and their strength increases with time until it gets saturated. The magnetic field strength is the highest in the center and expands to the central 10 pc region in about 1 Myr. Such strongly amplified and volume-filling magnetic fields favor the formation of massive black holes, as we discuss below.

### 3.2. Impact of Magnetic Fields on Disk Fragmentation

We find that self-gravitating accretion disks form at the center of each halo as a result of gravitational collapse in both HD and MHD simulations. The time evolution of disks in the simulated halos for both cases is shown in Figure 4. In general, the disks are more stable and have larger sizes in the MHD runs while they are more compact and gravitationally unstable in the HD runs. Overall, the degree of fragmentation is higher in the HD simulations. For the MHD runs, no fragmentation is observed in two out of three halos (halos 1 and 3) by the end of the simulations as only one clump forming over time gets merged with the central clump. In halo 2, two clumps are formed and survive for about 1 Myr for the MHD case (see Figure 5) and we expect these clumps to evolve into a binary system. On the other hand, in the HD runs the disks are more prone to fragmentation and multiple clumps form in them; some get subsumed in the center of the disk but a handful survive by the end of the simulations. The differences in fragmentation are due to the magnetic pressure (comparable to the thermal pressure) which increases the Jeans mass and stabilizes the disks. Consequently, initially more massive clumps form in the MHD runs.

We ran the YT clump finder (see Section 2 for details) to estimate the masses of the gravitationally bound clumps. The initial clump masses are estimated when they are found for the first time in the data output and are listed in Table 1 for both

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**Figure 3.** Average magnetic field strength along the x-axis within the central 10 pc. The columns show the time evolution of the magnetic field strengths for the simulations MH1, MH2, MH3, and LH1.
Figure 4. Average density along the x-axis within the central 10 pc for both the MHD and HD runs. The columns show the time evolution of the disk in the MHD and HD simulations.

Figure 5. Same as Figure 4 except that the central 2 pc view is shown.
MHD and HD runs. In general, the initial clump masses in HD cases are lower than their MHD counterparts, up to a factor of four in case of halo 2. But by the end of simulations, over a time span of 1.6 Myr, the clump masses in the HD runs become approximately comparable to those in MHD as a result of merging. For the MHD cases, only one clump forms in halos 1 and 3, two in halo 2, and they have typical masses of $\sim 10^5 M_\odot$. Multiple clumps exist in all halos in the HD runs and their masses range from a few thousands to about 100,000 solar. Overall, the central clumps are more massive than the secondary clumps. To comprehend the mass evolution of the central clumps and the differences in the central clump masses between the MHD and HD runs, we show the mass accretion rates and the masses of the central clumps in Figure 6. The mass accretion onto the clumps is intermittent in both cases and fluctuates about the average accretion rate of $\sim 0.1 M_\odot$ yr$^{-1}$. The peaks in the accretion rates correspond to the epochs when the clumps merge. In general, the mass accretion rates in the MHD runs are similar to the non-MHD cases. In MH1, the mean accretion rate onto the main clump is about a factor of 1.5 lower after the initial burst of accretion.

Although the initial masses of the central clumps in two out of three halos are larger in the MHD runs, the merging of secondary clumps in the HD simulations yields similar clump masses at the end of the simulations. For MH1, the initial bursts of accretion boost the clump mass to 100,000 solar during the first 500 kyr which gets doubled over the next megayear. In spite of an about 1.5 times higher accretion rate in H1, the formation of multiple clumps and tidal interactions among them disrupts the growth of central clump and consequently its mass is two times lower than for MH1. The tidal interaction of the clumps is evident from wiggles on the central clump mass plot. Contrary to MH1, binary clumps form within the first few hundred kiloyear in MH2 which result in about factor of two lower clump masses than the H2. On the other hand in H2, clumps forming during the first 400 kyr migrate inwards and boost the mass of the central clump which remains two times larger than MH2 by the end of the simulations. The secondary clumps in H2 form at later times and mainly grow through mergers. Overall, the mass accretion rate onto the main clumps is similar for both MH2 and H2. In MH3, although the initial clump mass is a factor of 2–3 larger than H2 during the first 500 kyr, multiple clumps merge over time in H3 boosting the central clump mass which becomes comparable to the MH3 case. In general, the masses of the main clumps in both MHD and HD cases are $\sim 10^5 M_\odot$, and their mass distribution at the end of the simulations is shown in Figure 7. The clump mass distribution is bimodal, the masses of the central clumps in both MHD and HD runs peak at $\sim 10^5 M_\odot$, while the masses of the secondary clumps mainly forming in HD runs have masses of $10^4 M_\odot$ except for one of the binary clumps in MH2. In Figure 8, we compare the migration timescale of the clumps from simulations with analytical estimates from Lin & Papaloizou (1986) given in Equation (17) of Latif & Schleicher (2015). We find that the migration timescales vary from a few times $10^7$–$10^8$ yr depending on the clump mass and its distance from the center of a disk. These estimates are in good agreement with analytical models and explain the migration of clumps within 1 Myr after their formation.

4. Discussion and Conclusions

We have investigated here the impact of magnetic fields on the formation of DCBHs by performing a suite of 3D MHD cosmological simulations for three distinct halos and have compared their results with HD runs. These simulation are evolved for 1.6 Myr, comparable to the expected lifetime of SMSs. For MHD simulations, we have taken a fiducial value of $10^{-15}$ G for the initial seed magnetic fields and also explored a case with $10^{-20}$ G. The simulated halos have masses of $10^7 M_\odot$ at $z \geq 12$. This study has enabled us to quantify the role of magnetic fields during the formation of SMSs.

We found that, irrespective of the initial field strength, magnetic fields get rapidly amplified in the presence of strong accretion shocks on timescales shorter than the freefall time and reach the saturation state. These results are comparable with previous findings of L14, G19, and Hirano et al. (2021). Such strongly amplified magnetic fields enhance the Jeans mass, stabilize the accretion disks, and significantly reduce fragmentation. Overall, disks are more stable and have larger sizes in MHD runs while a higher degree of fragmentation is observed in HD runs. In spite of lower initial clump masses in HD simulations, the higher clump merger rate yields masses of the central clumps similar to the MHD simulations. The masses of the central clumps are $\sim 10^5 M_\odot$, and the average mass accretion rate 0.1 $M_\odot$ yr$^{-1}$. They are similar for both the MHD and HD runs. Multiple secondary clumps are found in HD runs by the end of the simulations contrary to the MHD runs. In halo 2, two clumps survived for more than 1 Myr and they are expected to form a binary system.

We have employed here a pressure floor technique which stabilizes the collapse on the smallest scales and allows us to evolve simulations for longer times. This approach suppresses fragmentation on scales of a few times 0.01 pc. Alternatively sink particles are employed in the literature which represent gravitationally bound structures. We compared the results of the pressure floor method with sink particles in Latif et al. (2013c) and Latif et al. (2022b) and found that both methods yield similar results. These state-of-the-art methods are commonly employed in simulations but have their own limitations. The pressure floor technique may increase the minimum size of clumps and consequently enhance the clump merger rate, although higher-resolution simulations without pressure floors show that clumps migrate inwards on shorter timescales and merge with the central clump (Greif et al. 2011; Latif et al. 2013a; Sakurai et al. 2015; Hosokawa et al. 2016; Chon et al. 2018; Suazo et al. 2019). Also, such migration and merging of clumps is in agreement with theoretical models of disk fragmentation (Lin & Papaloizou 1986; Inayoshi & Haiman 2014; Latif & Schleicher 2015). On the other hand, contemporary star formation simulations show that sink creation depends on the choice of the threshold density, numerical resolution, accretion, and merging radii as well as on the recipe of sink formation (Guszejnov et al. 2018; Haugbolle et al. 2018). They further reveal that the sink mass distributions are not well converged unless simulations have higher spatial resolution, well resolved Jeans lengths and smaller merging radii. We expect our main conclusions to remain valid in spite of these caveats.

We have assumed here an isothermal collapse mediated by strong long-wave radiation. However at densities above $\gtrsim 10^6$cm$^{-3}$ radiative association of hydrogen atoms with electrons results in photon emission known as H$^-$ cooling.
Latif et al. (2016b) found that H$^-$ cooling decreases the gas temperature down to $\sim$5000 K and causes small-scale fragmentation; the clumps at these scales are expected to migrate inwards. Recently, Hirano et al. (2021) included this process in their idealized simulations of an atomically cooling gas cloud and found a higher degree of fragmentation, but most of the clumps were able to coalesce with main clump. Therefore, we expect that the inclusion of H$^-$ cooling will have little impact on our findings but future MHD cosmological simulations should include this process.

Figure 6. Mass accretion rates for the central 0.1 pc of the halo and the corresponding enclosed masses for the MHD and HD simulations. The solid lines represent the HD runs and the dashed lines the MHD runs.
Latif & Schleicher (2016) found that magnetic fields can launch jets and outflows from magnetized SMSs, consistent with duration of gamma-ray bursts (Butler et al. 2018; Sun et al. 2018) and may even impact the host galaxy. Whalen et al. (2020, 2021) estimated the radio emission from accreting DCBHs and found that they can be detected with upcoming radio observatories such as SKA and ngVLA.

M.A.L. thanks the UAEU for fundings via UPAR grants No. 31S390 and 12S111. D.R.G.S. gratefully acknowledges...
