Phase-stabilized UV light at 267 nm through twofold second harmonic generation

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Abstract: Providing phase stable laser light is important to extend the interrogation time of optical clocks towards many seconds and thus achieve small statistical uncertainties. We report a laser system providing more than 50 µW phase-stabilized UV light at 267.4 nm for an aluminium ion optical clock. The light is generated by frequency-quadrupling a fibre laser at 1069.6 nm in two cascaded non-linear crystals, both in single-pass configuration. In the first stage, a 10 mm long PPLN waveguide crystal converts 1 W fundamental light to more than 0.2 W at 534.8 nm. In the following 50 mm long DKDP crystal, more than 50 µW of light at 267.4 nm are generated. An upper limit for the passive short-term phase stability has been measured by a beat-node measurement with an existing phase-stabilized quadrupling system employing the same source laser. The resulting fractional frequency instability of less than 5 × 10⁻¹⁷ after 1 s supports lifetime-limited probing of the ²⁷Al⁺ clock transition, given a sufficiently stable laser source. A further improved stability of the fourth harmonic light is expected through interferometric path length stabilisation of the pump light by back-reflecting it through the entire setup and correcting for frequency deviations. The in-loop error signal indicates an electronically limited instability of 1 × 10⁻¹⁸ at 1 s.

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1. Introduction

Many applications in quantum physics require phase stable light sources. Optical clocks stand out for their stringent requirement on phase stability to achieve long interrogation times and thus small statistical uncertainties [1]. This is particularly important for single or few ion optical clocks, owing to their limited signal-to-noise ratio, requiring lifetime-limited interrogation times to achieve competitive statistical uncertainties [2–5]. Starting from lasers stabilized to ultra-stable cavities [6–24] that can provide coherence times exceeding 11 s [25], several schemes have been devised to even further extend the coherence time of the clock interrogation light by employing multiple ensembles of clocks [26–32]. To maintain the high phase coherence, the effect of disturbances on the probe light due to fluctuations of the refractive index caused by temperature or pressure variations within the optical medium (air or optical fibers) on the way towards the clock atoms must be eliminated. This is typically achieved through a Michelson interferometer, where a short reference arm is compared in a heterodyne measurement with the frequency-shifted laser radiation that has traveled through the medium and back again, with its frequency corrected by an acousto-optical frequency shifter [33,34]. However, several optical clock transitions are in the ultraviolet (UV) spectral range. Examples include the ²⁷Al⁺ ion quantum logic optical clock with a clock transition wavelength of 267 nm [35–42], the ¹⁹⁹Hg⁺ ion clock with a clock transition at 282 nm [35,43,44], the ¹¹⁵In⁺ ion clock operated at a wavelength of 237 nm [45–47], and the neutral atom mercury lattice clock at 266 nm [48–51]. The UV laser light in this wavelength regime is typically generated through fourth harmonic generation (FHG) of IR lasers. A common
method of FHG generation is given by twofold SHG in non-linear media often using pump-beam power enhancement in a cavity for high efficiency [52–67]. The challenge is to transfer the phase stability from the cavity-stabilized IR laser through all optical paths including the frequency doubling stages to the UV light. It has been shown that highly efficient single-pass waveguide doublers, converting IR radiation into the visible wavelength regime, do not introduce additional noise at a level of $10^{-19}$ [68,69]. However, waveguide doublers for conversion into the UV are not available. Frequency doubling systems employing a pump beam resonant enhancement cavity are expected to add negligible noise, since the optical path length of the pump beam within the cavity is stabilized by locking the cavity length to the pump beam wavelength [70]. Therefore, phase stabilization is required before, after and between the SHG units, including possible active elements, such as power amplifiers, which significantly increases the complexity of the setup.

Here we describe and characterize the generation of UV probe light for the $^{27}$Al$^+$ clock at 267.4 nm based on two cascaded single-pass SHG stages, significantly reducing the complexity of the setup and enabling continuous length stabilization of the optical path through back reflection of the IR light at the output of the UV doubling stage. Assuming that the intermediate frequency doubled and the target quadrupled light are common path and dispersion effects are small, we expect that phase stabilisation of the IR light path also provides phase stability of the UV light. We characterize the performance of the system in terms of output power and phase stability. The latter is quantified by a comparison with a conventional FHG setup with cascaded waveguide and cavity-enhanced SHG units, employing piecewise phase stabilisation.

2. Crystal selection

According to SHG theory, efficient harmonic generation requires a large nonlinear coefficient $d_{\text{eff}}$, phase matching between the fundamental (pump) and second harmonic field, and a good spatial overlap between these two fields. In the non-depleted pump regime and assuming plane wave interaction, the generated SHG intensity scales quadratically with the pump intensity $I_{\omega}$ [71]

$$I_{2\omega} \propto d_{\text{eff}}^2 I_{\omega}^2 \omega^2 \sin^2 (\Delta kl/2) / (\Delta kl/2)^2,$$

where $l$ is the length of the crystal, $\omega$ is the pump frequency and $\Delta k = k_{2\omega} - 2k_{\omega}$ is the difference between the wavenumbers of the pump and SHG fields. For strong conversion (pump depletion regime), the relation between SHG and pump intensity becomes linear. For phase-matched fields ($\Delta k = 0$), the generated SHG in each part of the crystal along the propagation direction is coherently added to the existing SHG field. There are several possibilities to achieve this, depending on the properties of the nonlinear crystal. Taking advantage of the birefringence of most nonlinear crystals, critical phase matching can be achieved through a proper choice of polarisation and angle of the incident fields with respect to the crystal axes. However, this results in the SHG field being emitted under an angle with respect to the pump field (walk-off), which reduces the spatial overlap between the fields and therefore SHG efficiency. Some nonlinear crystals offer a temperature-dependence of their refractive indices that enables phase matching within a certain wavelength range (non-critical, temperature, or 90° phase matching). In this case, the fields propagate along one of the crystal axis, avoiding walk-off. Finally, quasi-phase matching (QPM) enables an effective $\Delta k = 0$ through a periodic modulation of the sign of $d_{\text{eff}}$ along the propagation direction. The change in sign ensures that the generated SHG field continues to coherently add to the existing SHG field after running out of phase after a coherence length $l_c = 4(n_{2\omega} - n_{\omega})^{-1}$, where $\lambda$ is the fundamental wavelength and $n_{\omega}$ and $n_{2\omega}$ are the refractive indices of the fundamental and SHG field, respectively. This results in a $d_{\text{eff}}$ smaller by a factor of $2/\pi$ compared to non-critical phase matching. Boyd and Kleinmann have extended the SHG treatment to Gaussian beams [72], where absorption, divergence and walk-off limit the optimal crystal length and focus inside the crystal. The detrimental effects of Gaussian beam
divergence can be overcome by employing waveguide crystals [73–79], in which fundamental and harmonic fields are guided in a single transverse mode structure. Cascaded single-pass SHG with mode overlap between the fundamental and harmonic beams requires either QPM or non-critical phase matching, significantly limiting the crystal choices. We have therefore selected a periodically-poled lithium niobate (PPLN) ridge waveguide crystal, manufactured by HC Photonics Corp., for the first doubling stage from 1069.6 nm to 534.8 nm. The crystal has a length of 10.3 mm, is anti-reflection coated for both wavelengths, and achieves an intrinsic efficiency of ~125 % W⁻¹ at a phase-matching temperature of 45 ± 20°C, according to the manufacturer. The temperature of the QPM SHG crystal needs to be stabilized, since a change in temperature changes the refractive index and – through thermal expansion – the periodic poling period. For a waveguide the effective refractive index also depends on the geometry of the waveguide, which is not known to us. We therefore use the expected temperature tuning bandwidth ΔT=2.8 K cm of a bulk PPLN crystal [80] as a reference.

For the second doubling stage from 534.8 nm to 267.4 nm, we have chosen a 50 mm long deuterated potassium dihydrogen phosphate (DKDP) crystal, which allows non-critical phase matching at an expected temperature of around 100°C [81] and has a non-linear coefficient $d_{eff}$ ≈ 0.43 pm V⁻¹ [82]. The temperature tuning bandwidth of this crystal is given by 3.2 K cm [82]. The optimal focus waist of 32 μm [72] of the pump beam inside the crystal results in a calculated single-pass conversion coefficient of 0.15 % W⁻¹. In Tab. 1, the key parameters for both crystals are listed.

| Value                                      | PPLN | DKDP |
|--------------------------------------------|------|------|
| Length in mm                               | 10.8 | 50   |
| Facet dimensions in mm²                    | 0.5 x 1.5 | 5.0 x 5.0 |
| Transparency range bulk in nm              | 300...5000 | 200...2100 |
| Absorption coefficient pump light in cm⁻¹  | ≈ 0.003 | ≈ 0.004...0.005 |
| Absorption coefficient SHG in cm⁻¹         | ≈ 0.03 | ≈ 0.004...0.005 |
| $d_{eff}$ in pm V⁻¹                        | 14...16 | ≈ 0.43 |
| Conversion coefficient in % W⁻¹            | 125  | 0.15 |
| Hygroscopicity                             | none | high |
| Expected phase matching temperature in °C   | 45(20) | ≈100 |
| Temp. tuning bandw. in K cm                | 2.8  | 3.2  |
| Manufacturer                               | HCP  | Altechna |

### 3. Technical description of the setup

The FHG setup consists of two cascaded SHG stages. Each stage is placed inside a self-built oven for temperature control. The system is fibre coupled and a phase stabilisation scheme is included to compensate phase noise throughout most of the optical paths.
3.1. Mechanical design

The setup is built on a breadboard inside a hermetically sealed box of size of 42 cm x 23 cm x 8.5 cm, both made from aluminium (see Fig. 1), which makes it rigid and stable against external perturbations such as temperature, and pressure fluctuations and vibrations. Its compact design allows a high degree of transportability and the integration into a commercial 19 inch rack. The box is sealed with a Viton® ring and evacuation to avoid air fluctuations is possible via a flange on the lid. Alternatively, damaging of optical components due to UV light can be suppressed by purging the box with clean gas [83] for example oxygen or nitrogen. Optical access to the volume is provided by a number of windows which are sealed with indium. The fibre collimators for the two aforementioned optical fibers are mounted to the box from the outside in front of such windows. For focusing of the laser beam into the first SHG stage and recollimation after the first SHG stage non adjustable lenses are integrated in the first oven. For focusing the laser beam into the second stage with a specific beam waist, a telescope consisting of a concave and a convex lens is used. For recollimation an identical telescope in an inverted arrangement is used. All four lenses are mounted on individual linear translation stages to enable a precise adjustment along the direction of beam propagation. The optical power at all wavelengths can be monitored with photodiodes. The photodiodes are placed behind windows outside the box to avoid contamination from out-gassing of components of the photodiodes. All optical components like mirrors and (dichroic) beam-splitters are situated in either adjustable or fixed highly-stable mounts.
**Design of the ovens:** The ovens of both crystals share a similar design and provide an accurate, constant and homogenous phase matching temperature of up to 100 °C. A cut-away drawing of the first oven is shown in FIG. 2. In the first oven the waveguide (1) is placed inside a copper socket (2). To prevent mechanical stress and to ensure thermal contact, the waveguide is wrapped in a single 100 µm layer of indium foil. A spring-loaded copper plate is used to push the waveguide against the socket (3), while mechanical tension is avoided. Two Peltier elements (4) are used for heating. The temperature is measured by two PT1000 temperature sensors (5), one of which is integrated in the top part and the other in the bottom part of the socket. A PID controller is used to actively stabilise the oven temperature with a resolution of 0.001 °C using one of the two PT1000 temperature sensors. The other PT1000 temperature sensor is used as a monitoring sensor. The connection of the PT1000 temperature sensors and the Peltier elements with the PID controller (Meerstetter TEC-1091) are realized through a vacuum-compatible sealed d-sub multi-pin feed-through, which is integrated into the wall of the box. For thermal isolation of the oven the socket is surrounded by an inner shield made of MACOR® (6). The remaining temperature difference between the oven and the environment can lead to convection of the surrounding gas. The latter can result in optical power instabilities due to beam pointing fluctuations and phase distortions of the beam. This is suppressed by adding a second shield (7) to the oven. This outer shield is made of copper and is in thermal contact with the breadboard via the copper ground plate of the oven. The apertures for the pump laser beam and SHG beam in the outer shield are realized within an extension of the outer copper shield to further reduce fluctuation in the gas of the pump light path. The outer shield does not exceed 25 °C during normal oven operation. Two lenses (8) for coupling the IR light into the waveguide are directly integrated into the extrusion of the outer shield of the first oven.

The DKDB crystal is placed inside a similar oven. However, with 50 mm it is longer and thus the spatial homogeneity of the temperature is more critical. Therefore, three rows consisting of three Peltier elements and six PT1000 sensors, three in the bottom part of the socket and
three on the top part of the socket are employed. The two outer rows of Peltier elements operate in series on a fixed current. The current of the middle row Peltier elements is controlled by a PID controller for active temperature stabilisation using one of the PT1000 temperature sensor. The other PT1000 temperature sensors can additionally be used for separately monitoring the temperature inhomogeneity.

Different from the first oven, no lenses for mode matching are needed inside the second oven as the telescope before the oven serves that purpose. The performance of both ovens at their operational temperature is measured and shown in Tab. 2. This includes the long term temperature stability, the maximum heating or cooling ramp (limited for protection of the crystals), the temperature settling time (for temperature stability of < 0.05 °C) and the thermalization timescale (1/e time constant of an exponential approach).

### Table 2. Key parameters of the ovens for the nonlinear crystals.

| Measured value                  | PPLN-oven | DKDP-oven |
|---------------------------------|-----------|-----------|
| Operational temp.               | 44 °C     | 76 °C     |
| Long term temp. stability       | 0.01 °C   | 0.005 °C  |
| Max. temp. ramp                 | 1 °C/min  | 1 °C/min  |
| Temp. settling time             | 30 s      | 60 s      |
| Thermalization timescale        | (280 ± 30) s | (610 ± 30) s |

### 3.2. Optical setup

The optical set up is schematically depicted in FIG. 3. In our case the maximum input power is 1 W at 1069.6 nm. The IR light is delivered via a polarisation maintaining fibre to the first collimator outside the box. An AR-coated optical window transmits the light to the inside, where a polarizing beam splitter is used to clean the pump light polarization, resulting in a horizontal polarised pump light beam.

**First SHG stage from 1069.6 nm to 534.8 nm:** Two mirrors M1 and M2 are used to couple the beam into the PPLN waveguide. Mirror M1 is transparent at the backside allowing the transmitted light to be detected on a photodiode P1 outside the box for IR optical power monitoring. Lens L1 has a focal length \( f = +12.5 \) mm and is used to match the spatial mode of the pump light at 1069.6 nm to the waveguide with an NA of 0.16 in vertical and 0.14 in horizontal direction. The PPLN-ridge waveguide is placed inside the first oven. It efficiently converts the IR laser light at 1069.6 nm into green light at 534.8 nm via SHG when actively temperature stabilized at the phase matching temperature \( T_{pm} \approx 44 \) °C using type I phase matching. At 534.8 nm the NA of the waveguide is specified to be 0.8 in vertical and 0.7 in horizontal direction. The green light is horizontal polarized as two extraordinary photons are converted into one extraordinary with doubled frequency. The outgoing green and IR light beams are collimated with an achromatic AR-coated lens L2 with \( f = +12.5 \) mm, resulting in a diameter of 4 mm for IR light and 2 mm for green light.

**Second SHG stage 535 nm to 267 nm:** For high SHG efficiency of the second stage, the pump beam is focused in the centre of the crystal along its propagation direction. By solving the Boyd-Kleinman expression we find an optimal beam waist size of \( w_0 = 32 \) µm (radius at 1/e²
intensity level of the Gaussian beam at the focus point) for our given nonlinear crystal and 200 mW green pump light power. These calculated optimum focus position and waist for the green pump light are set by a telescope directly behind the first SHG. The telescope consists of two lenses \(L_3\) with \(f = -48\) mm and \(L_4\) with \(f = +75\) mm, which are placed on individual linear translation stages. The beam positioning between the first and second SHG stage can be adjusted with the two fold mirrors \(M_3\) and \(M_4\). The first mirror is backside-polished. Therefore, the pump light at 535 nm for the second SHG stage can be measured by the photodiode \(P_2\) placed outside the box.

The green light at 534.8 nm is converted into 267.4 nm in a 50 mm long DKDP crystal using type I phase matching. The crystal is AR coated for both wavelengths and is placed inside the oven, which ensures a homogeneous phase matching temperature along the crystal. The green light is still horizontal polarized, which corresponds to the ordinary polarization in relation to the crystal orientation. The generated UV light is vertical polarized, as two ordinary photons are converted into one extraordinary with doubled frequency.

After the DKDP crystal the beam is collimated again with an adjustable two-lens system with \(L_5\) and \(L_6\) on individual linear translation stages and the position is adjusted by two mirrors (\(M_{5,6}\)). The generated UV light power level is monitored by photodiode \(P_3\) after transmission through a backside-polished mirror \(M_7\) and a subsequent short pass optical filter to remove any residual green and IR light. In Fig. 3 two variants of the FHG setup are depicted. In variant 1 the setup with a fibre coupled UV output is used as a UV laser source. Here, the reflected light off \(M_7\) is split by a dichroic mirror \(D_1\) in its green and the IR light contribution in pass direction and its UV light contribution in reflection. The UV light leaves the box through a window and can e.g. be coupled into a fibre. Variant 2 shows the setup when it is used as a reverence for second UV laser source or when the frequency stability of the system is measured with a second UV laser source (see 5).
**IR light path length stabilisation:** The setup is designed for minimal phase noise of the produced UV light. The air sealed box minimises the phase noise contribution due to pressure and temperature fluctuations. For the temperature dependence of the air at the free-space optical path in the box, one can roughly calculate a phase shift of \(13 \text{rad K}^{-1} \) \([84]\) (1.3 \text{rad K}^{-1} for the IR light path, 3.6 \text{rad K}^{-1} for green light path and 8.9 \text{rad K}^{-1} for UV light path). For the pressure dependence the phase shift is \(4 \text{rad hPa}^{-1} \) \([84]\) (0.4 \text{rad hPa}^{-1} for the IR light path, 1.1 \text{rad hPa}^{-1} for green light path and 2.6 \text{rad hPa}^{-1} for UV light path). We do expect effective temperature changes inside the box of less than 10 mK per second and pressure changes of less than 0.1 Pa per second. The resulting phase stability is 0.13 \text{rad s}^{-1} for temperature changes and 0.004 \text{rad s}^{-1} for pressure changes. The corresponding fractional frequency change \(\gamma(t)\) can be calculated through

\[
\gamma(t) = \frac{\Delta \phi}{2 \pi f t},
\]

where \(f\) is the frequency of the light, resulting in \(\gamma(1 \text{s}) \approx 1.9 \times 10^{-17}\) for temperature changes and \(\gamma(1 \text{s}) \approx 6 \times 10^{-19}\) for pressure changes. On time scales of a few seconds, this poses no limitation to the frequency instability. However, for longer integration times phase stabilisation is necessary. In this setup an interferometric length stabilisation is realised with the IR light and includes both SHGs and the major part of the optical path of the setup. As the beams with all three wavelengths are spatially overlapping until they are separated by \(D_1\), we expect the beams to undergo similar phase and frequency disturbances. Therefore, the length stabilisation of the IR light path serves as a reference for the UV light for all common length changes. Taking the dispersion of the air into account, the remaining temperature-induced phase shift for UV light is approximately \(0.8 \text{mrad K}^{-1}\), while the pressure-induced phase shift for UV light is approximately \(0.2 \text{mrad hPa}^{-1}\) \([84]\). Assuming again temperature changes of 10 mK \text{s}^{-1} or 0.1 mK Pa\(^{-1}\), the remaining fractional frequency instability due to the temperature or pressure change in the air is \(1 \times 10^{-18}\) or \(3 \times 10^{-20}\) and thus no limitation for the anticipated clock operation. The IR length stabilisation is implemented according to the scheme shown in Fig. 3, variant 1. Therefore, the IR light is backreflected by a short pass dichromatic mirror \(D_2\), closely behind \(D_1\). The green light is transmitted by \(D_2\) and can be used outside the box through a window. The IR light takes the same path back to the first collimator \(C_1\) and is coupled back into the fibre. The IR light phase stabilisation path consists of an AOM to correct any frequency changes, a beamsplitter, a retro reflective mirror (\(M_4\)) for the reference arm and a photodiode \(P_4\) to measure the heterodyne beat signal between the reference and the signal arm of the interferometer. A phase locked loop between the measured beat signal and a reference frequency is closed by feeding the rf correction signal into the AOM.

4. Characterisation of the FHG UV light

4.1. Non-critical phase matching of the SHGs

Both SHG stages use non-critical phase matching which makes any converted output power sensitive to temperature variations of the nonlinear crystal. The temperature dependence on the output power is depicted in Fig. 4 for the first SHG stage (left) and the second SHG stage (right). For the first SHG the maximum green light output is given at an oven temperature of 48.5 °C with a full width half maximum (FWHM) of 2.2 °C. The theoretical value for a 10.3 mm long bulk crystal is 2.7 °C (see section 2). The smaller measured temperature tuning bandwidth compared to the theoretically expected value for a bulk crystal might arise from a different effective reflective index in the waveguide. The maximum output power for the second SHG stage is obtained at an oven temperature of 77.84 °C with a FWHM of 0.61 °C, which is in good agreement with the theoretically expected value of 0.62 °C, while the obtained oven temperature differs from our expectations (see section 2).
4.2. UV light power output

The optical power of the converted light from the first SHG at 534.8 nm and from the second SHG at 267.4 nm is measured as a function of pump light power at 1069.6 nm. The results are shown in Fig. 5. It should be noted that the optimum oven temperature changes with pump light power as a consequence of additional crystal heating due to absorption. This is taken into account by optimizing the phase-matching temperatures of the two ovens for each pump power value individually. The IR pump light power of 1 W is converted into more than 200 mW green light by the first SHG and into more than 50 µW UV light power by the second SHG. For continuous operation of the FHG system, the green light output power should be limited to 200 mW to avoid damage of the waveguide due to the photorefractive effect and green light induced infrared absorption [85]. As shown in Section 3, the SHG light power scales quadratically with the pump light power in the low intensity regime. Therefore, the data in Fig. 5 are fitted with a quadratic function for the first SHG stage, taking only data with green light power output of less than 120 mW into account. We found a conversion coefficient of $\kappa = 119 \% \ W^{-1}$, which is close to the conversion coefficient of $\kappa = 125 \% \ W^{-1}$ stated by the manufacturer. For higher power, pump beam depletion results in a linear scaling. For the FHG generation, the data is fitted to a function of fourth power, taking the same data as before into account. Only considering the second SHG stage, the UV light power output is a quadratic function of the green pump light as shown in the inset of Fig. 5. Due to the low pump light power all data agree well with the quadratic fit. The conversion coefficient is $\kappa = 0.12 \% \ W^{-1}$, which is close to the theoretical maximal value of $\kappa = 0.15 \% \ W^{-1}$. Additionally, the output UV light power stability is measured for IR pump light power of 800 mW over 10 h. The measured UV output power of approximately 30 µW is stable within a range of 1 µW, mainly limited by the power stability of the pump light laser.
5. UV light frequency stability

The system described is designed for high passive frequency stability and at the same time offers the possibility of active stabilisation. In the following we refer to this system as system A. For characterising the passive phase stability a beat-note measurement with an existing quadrupling system B is performed, see Fig. 6. In this measurement, both laser signals are generated by the same fibre laser source. Therefore noise from the laser source itself is suppressed, since it is common to both arms. However, vibrations and temperature fluctuations can introduce optical path length variations in the reference system, which can significantly diminish the measured frequency stability and must be compensated for.

5.1. Setup for frequency stability measurement

For the measurement of the phase stability variant 2 in Fig. 3 is used. Here the outcoupling collimator C₂ is removed and the UV light generated by system B enters the box through this port. The dichromatic mirror D₁ is replaced by a partially reflective window, which is used to overlap part of the light from both systems. However, most of the UV light from system B is transmitted by the glass plate and is backreflected by D₁, which serves as the reference mirror for the last part of the phase stabilisation scheme of system B. The overlapping UV light inside the box is separated by the dichromatic mirror D₃ from the residual IR and green light and the beat-note of the UV light between system A and B is measured by the photodiode PD₅.

5.2. The reference UV laser source

The laser source for both systems is a fiber laser oscillator with an instantaneous linewidth of 10 kHz whose output is amplified by a fiber amplifier. The common path between both setups
ends at the polarising beamsplitter PBS$_1$ of Fig. 6 and some of the power is sent to system A (single-pass FHG). About 600 mW are coupled into reference system B through a 5 m long unstabilised fiber. An additional fiber amplifier in this system requires a special phase stabilisation scheme, since the amplifier cannot be operated bidirectional. Therefore, the light transmitted through BS$_1$, AOM$_1$, the fiber amplifier and the fiber-coupled waveguide doubler (SP-SHG) must be phase-stabilized. For this, the IR reflection off dichroic mirror D is interfered with the reflection from mirror Ref$_{1070\text{nm}}$, which acts as the reference mirror for phase stabilisation of the 1069 nm light. By keeping the optical path between the fiber output, D and Ref$_{1070\text{nm}}$ at a minimal length and enclosed in a compact optical bench system, the phase at the reference point at Ref$_{1070\text{nm}}$ coincides with the phase of the fiber output and is transferred to the green light at dichroic mirror D. The paths from Ref$_{1070\text{nm}}$ and D interfere on BS$_2$ and the beat-note is measured by PD$_{1070\text{nm}}$. A tracking oscillator filters the beat-note, which is phase-locked to a stable reference frequency by driving AOM$_1$ via a tunable direct digital synthesis (DDS) rf source. A second output of the tracking oscillator is counted using a dead-time free frequency counter.

The second doubling stage of system B is based on a pump-beam resonant SHG cavity. Since multi-path interference prevents stabilisation of the green light through the cavity, optical paths before and after the SHG cavity are separately length stabilised, paying attention to keep the unstabilised optical paths as short as possible.

About 172 mW at 534.8 nm of the waveguide’s output is transmitted by the dichroic mirror D and sent through free-space AOM$_2$ into a pump-beam resonant bow-tie cavity, where about 4 mW at 267 nm is generated in a BBO crystal. The length of the cavity is controlled by feedback onto a piezo mirror inside the cavity, using light at 535 nm reflected from the cavity’s input window in a Hänsch-Couillaud locking scheme [86]. Since multi-path interference prevents stabilisation of the green light through the cavity, optical paths before and after the SHG cavity are separately length stabilised, paying attention to keep the unstabilised optical paths as short as possible. In front of the cavity a small fraction of green light is back reflected onto PD$_{534.8\text{nm}}$, closing the path length stabilisation loop between reference mirror and retro-reflector by steering the frequency of AOM$_2$. The UV light generated in the cavity is frequency shifted by AOM$_2$, then enters system A. Here a fraction of the light is backreflected and brought into interference with
Fig. 7. Measurements of the fractional frequency instability of the FHG system expressed as the modified Allan deviation. The blue (yellow) line results from a beat-note measurement with the unstabilised (stabilised) external UV source (system B), representing an upper fractional frequency instability limit for the single-pass FHG system. The green line shows the free-running signal of the interferometric phase stabilisation scheme divided by two without active phase stabilisation. A lower bound is given by electronic measurement noise of the in-loop error signal of the active phase stabilisation (red line). For comparison, the lifetime-limited quantum projection noise limit of the clock transition of $^{27}$Al$^+$ at 267.4 nm is given as the dashed black line (see text for details).

At the point of PD$_5$ the light from system B has accumulated a frequency offset of $f_B - f_A = 251$ MHz with respect to $A$. The beat signal from the photodiode is amplified and filtered by an tracking oscillator and counted by a dead-time free frequency counter.

5.3. Results of UV light frequency stability measurement

To determine an upper bound for the frequency stability of the UV light the beat signal between the two systems is recorded for several hours, while system B is either phase stabilised or unstabilised. System A (the single-pass FHG) is not phase stabilised during the measurements. Fig. 7 shows the modified Allan deviation [87] of the recorded fractional frequency difference. For an averaging time of 1 s a fractional frequency instability limit of $1 \times 10^{-15}$ is measured for the unstabilised systems (blue line). With reference system B stabilised (yellow line) the fractional frequency instability limit reaches $5 \times 10^{-17}$ at a averaging time of 1 s, reaching down to $10^{-18}$ for gate times of $10^3$ s.

5.4. In-Loop phase noise measurement of the single-pass FHG

For a further assessment of the intrinsic phase stability of the FHG, the interferometric phase stabilisation scheme as discussed in section 3.2 and shown in Fig. 3, variant 1 is set up. The free-running signal of this interferometric phase stabilisation scheme is counted without active phase stabilisation. As the interferometric path contains any phase shift twice, we divide the
result by two. From the data the modified Allan deviation of the fractional frequency instability is calculated. The result as shown in Fig. 7 (green line) gives the fractional frequency instability of the passive stability of the FHG system. At an integration time of 1 s we find for the fractional frequency instability $7 \times 10^{-17}$, which is in good agreement with the previous measurement using the stabilised external UV light source (system B) as a reference. For longer averaging times the fractional frequency stability of the free-running signal is lower compared to the measured fractional frequency instability measured with the reference system. This could either indicate a limitation of the phase stability of the reference system or is caused by different lab conditions during the measurements. Also remaining non-stabilised fibers in both systems in Fig. 6 are likely to limit the measurement at the observed level. As the FHG setup is designed to be used to probe the clock transition of an $^{27}$Al$^+$ ion, we compare our results to its quantum projection noise limit [3] using Ramsey spectroscopy with a probe time corresponding to the excited state lifetime of 20.6 s [41] (dashed black line in Fig. 7). The fractional frequency instability of the passive FHG system is already below the quantum projection noise limit. We expect further improvements of the phase stability of the FHG setup with active phase stabilisation. The measurement of the residual in-loop signal of the active phase stabilisation scheme (red) provides a lower bound to the achievable fractional frequency instability. The signal to noise ratio was below 40 dB. For an independent verification of the performance of the stabilised system, two independent systems at this performance level would be necessary.

6. Conclusion

The demonstrated single-pass FHG system has demonstrated exceptional phase stability while the provided output power is expected to be sufficient for probing clock transitions. In case more power is required while maintaining phase stability, the single-pass FHG system can act as a phase reference for a separate and more efficient enhancement cavity-based FHG system. An upper bound to the passive phase stability of the unstabilised setup is obtained by a frequency comparison with a stabilised external UV light source and by observing the free-running signal of the interferometric phase stabilisation loop. Both measurements show a phase stability close to the lifetime-limited quantum projection noise limit of an aluminium ion clock with a 8 mHz narrow clock transition. Active phase stabilisation has been implemented and is expected to decrease the fractional frequency instability of the system further.

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Data availability. Data underlying the results presented in this paper are not publicly available at this time but may be obtained from the authors upon reasonable request.

References

1. A. D. Ludlow, M. M. Boyd, J. Ye, E. Peik, and P. Schmidt, “Optical atomic clocks,” Rev. Mod. Phys. 87, 637–701 (2015).
2. I. D. Leroux, N. Scharnhorst, S. Hannig, J. Kramer, L. Pelzer, M. Stepanova, and P. O. Schmidt, “On-line estimation of local oscillator noise and optimisation of servo parameters in atomic clocks,” Metrologia 54, 307 (2017).
3. E. Peik, T. Schneider, and C. Tamm, “Laser frequency stabilization to a single ion,” J. Phys. B: At. Mol. Opt. Phys. 39, 145–158 (2006).
4. E. Riis and A. G. Sinclair, “Optimum measurement strategies for trapped ion optical frequency standards,” J. Phys. B: At. Mol. Opt. Phys. 37, 4719–4732 (2004).
of phase noise introduced by an optical fiber or other time-varying path," Opt. Lett. 19, 1777–1779 (1994).
35. T. Rosenband, D. B. Hume, P. O. Schmidt, C. W. Chou, A. Brusch, L. Lorini, W. H. Oskay, R. E. Drullinger, T. M. Fortier, J. E. Stalnake, S. A. Diddams, W. C. Swann, N. R. Newbury, W. M. Itano, D. J. Wineland, and J. C. Bergquist, “Frequency ratio of 199Hg+ and 199Hg single-ion optical clocks; metrology at the 17th decimal place," Science 319, 1808–1812 (2008).
36. S. M. Brewer, J.-S. Chen, A. M. Hankin, E. R. Clements, C. W. Chou, D. B. Hume, and D. R. Leibrandt, “27Al quantum-logic clock with a systematic uncertainty below 10−18," Phys. Rev. Lett. 123, 033201 (2019). Publisher: American Physical Society.
37. E. R. Clements, M. E. Kim, K. Cui, A. M. Hankin, S. M. Brewer, J. Valencia, J.-S. Chen, C.-W. Chou, D. R. Leibrandt, and D. B. Hume, “Lifetime-limited interrogation of two independent 27Al clocks using correlation spectroscopy," Phys. Rev. Lett. 125, 243602 (2020).
38. C. W. Chou, D. B. Hume, J. C. J. Koelemeij, D. J. Wineland, and T. Rosenband, “Frequency comparison of two high-accuracy 27Al optical clocks," Phys. Rev. Lett. 104, 070802 (2010). Publisher: American Physical Society.
39. D. Leibrandt, S. Brewer, J.-S. Chen, A. Hankin, D. Hume, D. Wineland, and C.-W. Chou, “Trapped-ion optical atomic clocks at the quantum limits," in Proceedings of the 48th Annual Precise Time and Time Interval Systems and Applications Meeting, Monterey, CA. (2017).
40. K.-F. C. Si-Jia Chao and K.-F. C. Si-Jia Chao, “Observation of 1S0 → 3P0 transition of a 86Ca+–27Al+ quantum logic clock," Chin. Phys. Lett. 36, 120601 (2019).
41. T. Rosenband, P. O. Schmidt, D. B. Hume, W. M. Itano, T. M. Fortier, J. E. Stalnake, K. Kim, S. A. Diddams, J. C. J. Koelemeij, J. C. Bergquist, and D. J. Wineland, “Observation of the 1S0 → 3P0 clock transition in 27Al," Phys. Rev. Lett. 98, 220801 (2007). Publisher: American Physical Society.
42. H. Leopardi, K. Beloy, T. Bothwell, S. M. Brewer, S. L. Bronley, J.-S. Chen, S. A. Diddams, R. J. Fasano, Y. S. Hassan, D. B. Hume, D. Kedar, C. J. Kennedy, D. R. Leibrandt, A. D. Ludlow, W. F. McGrew, W. R. Milner, D. Nicolodi, E. Oelker, T. E. Parker, J. M. Robinson, S. Romisch, J. A. Sherman, L. Sonderhouse, J. Yao, J. Ye, X. Zhang, and T. M. Fortier, “Measurement of the 27Al and 87Sr absolute optical frequencies," Metrologia 58, 015017 (2021). Publisher: IOP Publishing.
43. S. A. Diddams, T. Udem, J. C. Bergquist, E. A. Curtis, R. E. Drullinger, L. Hollberg, W. M. Itano, W. D. Lee, C. W. Oates, K. R. Vogel et al., “An optical clock based on a single trapped 199Hg+ ion," Science 293, 825 (2001).
44. W. Oskay, S. Diddams, E. Donley, T. Fortier, T. Heavner, L. Hollberg, W. Itano, S. Jefferts, M. Delaney, K. Kim, F. Levi, T. Parker, and J. Bergquist, “Single-atom optical clock with high accuracy," Phys. Rev. Lett. 97, 020801 (2006).
45. N. Ohtsubo, Y. Li, K. Matsubara, T. Ido, and K. Hayasaka, “Frequency measurement of the clock transition of an indium ion sympathetically-cooled in a linear trap," Opt. Express 25, 11725–11735 (2017).
46. N. Ohtsubo, Y. Li, N. Nemitz, H. Hachisu, K. Matsubara, T. Ido, and K. Hayasaka, “Frequency ratio of an 115In+ ion clock and a 87Sr optical lattice clock," Opt. Lett. 45, 5950–5953 (2020). Publisher: Optical Society of America.
47. Y. Wang, R. Dumke, T. Liu, A. Stejskal, Y. Zhao, J. Zhang, Z. Lu, L. Wang, T. Becker, and H. Walther, “Absolute frequency measurement and high resolution spectroscopy of 115In+ 5S1/2 1S0 – 5S5/2 3P0 narrowline transition," Opt. Commun. 273, 526–531 (2007).
48. J. J. McFerran, L. Yi, S. Mejri, S. Di Manno, W. Zhang, J. Guéna, Y. Le Coq, and S. Bize, “Neutral atom frequency reference in the deep ultraviolet with fractional uncertainty=5.7 × 10−15," Phys. Rev. Lett. 108, 183004 (2012).
49. N. Ohmnae, F. Bregolin, N. Nemitz, and H. Katori, “Direct measurement of the frequency ratio for hg and yb optical lattice clocks and closure of the hg/yb/sr loop," Opt. Express 28, 15112–15121 (2020). Publisher: Optical Society of America.
50. M. Takamoto, I. Ushijima, M. Das, N. Nemitz, T. Ohkubo, K. Yamanaka, N. Ohmnae, T. Takano, T. Akatsuka, A. Yamaguchi, and H. Katori, “Frequency ratios of sr, yb, and hg based optical lattice clocks and their applications," Comptes Rendus Physique (2015).
51. K. Yamanaka, N. Ohmnae, I. Ushijima, M. Takamoto, and H. Katori, “Frequency ratio of 199Hg+ and 87Sr optical lattice clocks beyond the SI limit," Phys. Rev. Lett. 114, 230801 (2015).
52. K.-H. Ko, Y. Kim, H. Park, Y.-H. Cha, T.-S. Kim, L. Lee, G. Lim, J. Han, K.-H. Ko, and D.-Y. Jeong, “High-power continuous-wave tunable 544- and 272-nm beams based on a diode-oscillator fiber-amplifier for calcium spectroscopy," Appl. Optics 120, 233–238 (2015).
53. H.-Y. Lo, J. Alonso, D. Kienzler, B. C. Keitch, L. E. d. Clercq, V. Negnevitsky, and J. P. Home, “All-solid-state continuous-wave laser systems for ionization, cooling and quantum state manipulation of beryllium ions," Appl. Phys. B 114, 17–25 (2014).
54. Z. Wang, F. Yang, G. Zhang, Y. Bo, S. Liu, S. Xie, Y. Xu, N. Zong, F. Li, B. Liu, J. Xu, Q. Peng, J. Zhang, D. Cui, Y. Wu, and Z. Xu, “High-power ultraviolet 278 nm laser from fourth-harmonic generation of a nd:YAG laser in CdB6," Opt. Lett. 37, 2403–2405 (2012). Publisher: Optical Society of America.
55. D. B. Hume, “Two-species ion arrays for quantum logic spectroscopy and entanglement generation," Ph.D. thesis, University of Colorado (2010).
56. S. Hamig, J. Mielke, J. A. Fenske, M. Misera, N. Beev, C. Ospelkaus, and P. O. Schmidt, “A highly stable monolithic enhancement cavity for second harmonic generation in the ultraviolet," Rev. Sci. Instruments 89, 013106 (2018). _eprint: https://doi.org/10.1063/1.5005515.
57. T. Schmitt, T. A. Puppe, A. Nendel, F. Lison, W. G. Kaenders, and M. Le Flohic, “Single mode tunable all solid-state
70. M. Abdel-Hafiz, P. Ablewski, A. Al-Masoudi, H. A. Martínez, P. Balling, G. Barwood, E. Benkler, M. Bober, J.S. Sun and C. Xu, “466 mW green light generation using annealed proton-exchanged periodically poled MgO:LiNbO3,” Opt. Express 29, 37140–37149 (2021). Publisher: Optical Society of America.

71. G. D. Boyd and D. A. Kleinman, “Parametric interaction of focused gaussian light beams,” J. Appl. Phys. 39, 3579–3639 (1968). eprint: https://doi.org/10.1063/1.1656831.

72. G. D. Boyd, A. Ashkin, J. M. Dziedzic, and D. A. Kleinman, “Second-harmonic generation of light with double refraction,” Phys. Rev. 137, A1305–A1320 (1965). Publisher: American Physical Society.

73. G. D. Boyd and D. A. Kleinman, “Parametric interaction of focused gaussian light beams,” J. Appl. Phys. 39, 3579–3639 (1968). eprint: https://doi.org/10.1063/1.1656831.

74. K. A. Fedorova, G. S. Sokolovskii, M. Khomylev, D. A. Livshits, and E. U. Rafailov, “Efficient yellow-green light generation at 544 nm by frequency-doubling of a QD-FBG laser diode in a PPLN waveguide,” Opt. Lett. 34, 3511–3513 (2009).

75. S. Suntsov, C. E. Rüter, D. Brüske, and D. Kip, “Watt-level 775 nm SHG with 70% conversion efficiency and 97% pump depletion in annealed/reverse proton exchanged doped PPLN ridge waveguides,” Opt. Express 29, 11380–11393 (2021). Publisher: Optical Society of America.

76. C.-Y. Cho, J.-Y. Lai, J.-Y. Lai, C.-S. Hsu, Y.-T. Huang, J.-H. Jang, and M.-H. Chou, “Power scaling of continuous-wave second harmonic generation in a MgO:PPLN ridge waveguide and the application to a compact wavelength conversion module,” Opt. Lett. 46, 2852–2855 (2021). Publisher: Optical Society of America.

77. K. A. Fedorova, G. S. Sokolovskii, M. Khomylev, D. A. Livshits, and E. U. Rafailov, “Efficient yellow-green light generation at 561 nm by frequency-doubling of a QD-FBG laser diode in a PPLN waveguide,” Opt. Lett. 39, 6672–6674 (2014). Publisher: OSA.

78. M. M. Fejer, G. A. Magel, D. H. Jundt, and R. L. Byer, “Quasi-phase-matched second harmonic generation: tuning and tolerances,” Quantum Electron. IEEE J. 28, 2631–2654 (1992).

79. D. N. Nikogosyan, Nonlinear Optical Crystals: A Complete Survey (Springer, 2005).
82. “SNLO (free version),”.
83. H. Schröder, P. Wagner, D. Kokkinos, W. Riede, and A. Tighe, “Laser-induced contamination and its impact on laser damage threshold,” in Laser-Induced Damage in Optical Materials: 2013, vol. 8885 (International Society for Optics and Photonics, 2013), p. 88850R.
84. B. Edlén, “The Refractive Index of Air,” Metrologia 2, 71–80 (1966).
85. J. Sun and C.-q. Xu, “Green-induced infrared absorption in annealed proton-exchanged MgO:LiNbO3 waveguides,” J. Opt. Soc. Am. B 31, 2779–2785 (2014). Publisher: OSA.
86. T. W. Hänsch and B. Couillaud, “Laser frequency stabilization by polarization spectroscopy of a reflecting reference cavity,” Opt. Commun. 35, 441–444 (1980).
87. E. Benkler, C. Lisdat, and U. Sterr, “On the relation between uncertainties of weighted frequency averages and the various types of allan deviations,” Metrologia 52, 565–574 (2015). Publisher: IOP Publishing.