High-Performance Nano-Sensing and Slow-Light Applications Based on Tunable Multiple Fano Resonances and EIT-Like Effects in Coupled Plasmonic Resonator System

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ABSTRACT A basic plasmonic system, consisting of a stub metal-insulator-metal (MIM) waveguide coupled with a ring resonator, is presented to realize Fano resonance and electromagnetically induced transparency-like (EIT-like) effect, which are numerically calculated by the finite element method (FEM). Meanwhile, the formation mechanism of Fano resonance is analyzed according to numerical simulations. Besides, the coupled mode theory (CMT) and the standing wave theory are used for explaining the Fano and EIT-like resonances phenomenon. Based on this system, an inner ring cavity is connected to the ring resonator by a slot and another ring cavity is later introduced under the stub resonator in order to constitute a new coupled plasmonic resonator system, providing quadruple Fano resonances and double EIT-like responses finally. In addition, the Fano and EIT-like resonances can be independently tuned by adjusting the structural parameters, which makes the design of highly integrated photonic circuits more flexible. The main contribution of this paper is that the proposed structure has a relatively good sensitivity of 1600 nm/RIU and an ultra-high FOM value of $1.2 \times 10^6$ as a refractive index nanosensor. Moreover, it can serve as an all-optical switch with a high on/off extinction ratio of about 43 dB. Additionally, its maximum group delay time and group index are about 1.49 ps and 221, indicating that the proposed system has a pretty good slow light effect. Therefore, the proposed structures are believed to have significant applications in high-performance nanosensors, switches, slow light devices and nonlinear areas in highly integrated plasmonic devices.

INDEX TERMS Multiple EIT-like effects, multiple Fano resonances, refractive index sensor, surface plasmon polaritons (SPPs), slow light, ultra-high FOM.

I. INTRODUCTION

With the development of optical technology, future integrated optics will have higher requirements on the density of integration. Surface plasmon polaritons (SPPs), which can control the propagation of optical signal in nanoscale because of their strong field confinement to the interface of the metal and dielectric [1], [2], show a great prospect in the application of subwavelength optical devices and highly integrated photonic circuits [3].

So far, there have been numerous SPPs guiding structures like metal nanoparticle waveguides, metal films [4], metal-insulator-metal (MIM) slabs [5]–[8], plasmonic nanoclusters [9], [10], nano-slits [11], and hybrid Bragg waveguides, among which the MIM waveguide has the advantages of deep-subwavelength confinement [12], low bend losses [18] and easy integration [13], [14]. Therefore, it has crucial applications in highly integrated optical devices [15]–[17]. Based on the MIM waveguide, enormous devices, like plasmonic nanosensors [18]–[21], slow light devices [22]–[24], all-optical switches [25], filters [26], splitters [27], and demultiplexers [28] have been investigated in theory and simulation. Among them, plasmonic nanosensing was rated as one of the top ten emerging technologies by Scientific American in 2018 [29]. Therefore, a growing number of researches are focusing on designing high-performance nano-sensors in MIM waveguide coupled resonators. Some novel physical features like Fano resonance...
and electromagnetically induced transparency (EIT)-like effect [30], [31] have important applications in refractive index sensors, because a tremendous linear shift of EIT-like and Fano resonance can be caused by a minimal environmental change [31]. Fano resonance is the coupling effect arising from the interaction between narrow discrete states (dark modes) and broad continuous state (bright mode) [32]–[34]. The Fano resonance can also be originally deemed as the classical analogue of EIT under certain conditions [35].

In comparison with Fano resonance, EIT is a quantum interference phenomenon with a narrow optical enhanced transmission spectrum as a result of the quantum destructive interference between the atomic resonances [36]. Previous researches indicate that an optical phenomenon similar to EIT, which is termed as EIT-like effect, can occur in the coupled plasmonic resonator system [37]. As a quantum interference effect [38], [39], EIT is exceedingly sensitive to alteration in the refractive index. Consequently, the EIT-like and Fano resonances show great potential in high-performance plasmonic sensors [40]. When it comes to the sensor, its sensitivity and figure of merit (FOM) are vital for evaluating the sensing performance of the system.

In this research, tunable multiple Fano and EIT-like resonances with a great sensitivity and a large FOM value are achieved in coupled plasmonic resonator system. First of all, a plasmonic system consisting of a stub MIM waveguide and a ring resonator is designed as a basic structure. The transmission spectrum, the phase shift and magnetic field $H_z$ distributions are numerically calculated in COMSOL Multiphysics by the finite element method (FEM). Meanwhile, the formation mechanism of Fano resonance is analyzed based on the transmission spectra and magnetic field distribution. Moreover, the transmission property can be well fitted by the coupled mode theory (CMT). According to the standing wave theory, Fabry-Perot (FP) cavity theory and TM mode theory, the resonant order $N$ is calculated by formulas and corresponds well with the numerical results in simulations.

Based on the basic structure, an inner ring cavity is connected to the ring resonator by a slot, and a ring cavity is later placed under the stub resonator to create a new coupled plasmonic structure, providing quadruple Fano resonances and double EIT-like effects, finally. Additionally, these multiple Fano and EIT-like resonances can be independently controlled by adjusting the dimensions of the slot or inner ring cavity since they stem from different mechanisms. Simulation results also indicate that the new system can act as an excellent nanosensor with a great sensitivity of 1600 nm/RIU and an ultra-high FOM of $1.2 \times 10^6$ and an optical switch with a high extinction ratio of about 43 dB which is higher than that of the optical switch in the references [7], [59], [60]. In comparison with the recent works [6], [7], [18]–[21], [40]–[45], [53], [55], our nanosensor performs better than most of them. Besides, a maximum group delay time and group index about 1.49 ps and 221 can be realized, which outperform the slow light devices in the references [20], [54]–[57]. Based on the ultra-high FOM, independent tunability and favorable expansibility of the multiple Fano and EIT-like effects, the proposed structure with its outstanding performance can be applied to highly integrated photonic devices, such as bio-chemical sensors, slow light devices, optical switches and filters.

II. STRUCTURE MODEL AND THEORETICAL ANALYSIS

The basic proposed structure is displayed in figure 1, and consists of a stub MIM waveguide coupled to a ring resonator. The gray part of the two-dimensional diagram represents silver, and the white etches in between are filled with air. The total length of the proposed structure is $D$, and the height of the stub is $H$. The center of the ring is $O_1$. The dimensions are fixed as: $D = 2 \text{ um}$, $H = 150 \text{ nm}$, $R = 250 \text{ nm}$, $\overline{R} = 225 \text{ nm}$, which further simplifies the calculation. Due to the restriction of the nanofabrication techniques the coupling distance between the stub resonator and the composite structure $g$ is chosen to be 10 nm. The widths of the MIM waveguide and the stubs, and the thickness of the ring cavity are all set to $w = 50 \text{ nm}$ so as to allow only the fundamental mode ($\text{TM}_0$) to propagate in the structure.

To explore the optical properties of the basic system, its transmission spectra are numerically calculated by FEM, which is displayed in figure 2. And it reveals that the system exhibits the Fano resonance and EIT-like response at 680 and 989 nm, called FR and EIT. Additionally, the transmittance of SPPs is expressed as $T = P_{\text{with}} / P_{\text{without}}$, here $P_{\text{with}}$ and $P_{\text{without}}$ stand for the SPPs power flows of the port with and without ring cavity, respectively [44]. And the dispersion relation of the TM mode is given as [47]:

$$\varepsilon_m k_d \tanh \left( \frac{w d_k}{2} \right) + \varepsilon_d k_m = 0 \quad (1)$$

And $k_d$ and $k_m$ are

$$k_d = \sqrt{\beta^2 - \varepsilon_d k_0^2}, \quad k_m = \sqrt{\beta^2 - \varepsilon_m k_0^2} \quad (2)$$

$$n_{\text{eff}} = \frac{\beta}{k_0} \quad (3)$$

where $k_d$ and $k_m$ are transverse propagation constants in air and silver, separately. $k_0$ is the free space wave vector. $\beta$ is the propagation constant of the SPPs wave. $n_{\text{eff}}$ is the effective refractive index of the SPPs in the MIM waveguide. $\varepsilon_d$ and $\varepsilon_m$ are the dielectric constants of the dielectric air ($\varepsilon_d = 1.0$) and the metal silver, separately. To describe the silver analytically, Drude model [46] is adopted and later implemented in the
software by interpolation. The model gives the permittivity of the silver in relation to the frequency as such:

\[
\varepsilon_m(\omega) = \varepsilon_\infty - \frac{\omega_p^2}{\omega^2 + i\omega\gamma},
\]

where \(\varepsilon_\infty = 3.7\), \(\omega_p = 9.1\text{eV}\), and \(\gamma = 0.018\text{eV}\).

The resonance wavelength of MIM waveguide coupled resonator can be derived on the basis of the standing wave theory \([28], [48]\) as

\[
\lambda = \frac{2n_{\text{eff}}L}{N - \phi/\pi}, \quad N = 1, 2, 3 \ldots
\]

Here \(L\) is the length of the resonator, \(N\) is the resonant order, \(\phi\) is the phase shift brought about by the SPPs reflection off the metal wall in the resonator. Based on equations (2)-(3), the \(n_{\text{eff}}\) can be derived as

\[
n_{\text{eff}} = \sqrt{\left[\varepsilon_m + \left(\frac{k_m}{k_0}\right)^2\right]} \quad (6)
\]

In order to analyze the Fano resonance and EIT-like effect, the CMT is used for explaining the transmission property. The amplitudes of the input and output SPPs waves of the resonator are denoted by \(S_{11+}, S_{11-}, S_{12+}, S_{12-}, S_{21+}\), and \(S_{21-}\), which are depicted in figure 1(b). When the SPPs wave with a frequency \(\omega\) is launched into the system from the input port of the MIM waveguide \((S_{12-} = 0)\), the time evolution of the field amplitude \(A_1\) of the stub resonator can be expressed as \([52], [53]\):

\[
\frac{dA_1}{dt} = \left(-j\omega_1 - \frac{1}{\tau_0} - \frac{1}{\tau_1} - \frac{1}{\tau_2}\right)A_1 + \kappa_1 e^{j\theta_1}S_{11+} + \kappa_2 e^{j\theta_2}S_{21+} \quad (7)
\]

\[
S_{21+} = \delta e^{j\phi_1}S_{21-} \quad (8)
\]

\[
S_{12-} = S_{11+} - \kappa_1 e^{-j\theta_1}A_1, \quad \kappa_1 = \frac{1}{\tau_1} \quad (9)
\]

\[
S_{21-} = -S_{21+} + \kappa_2 e^{-j\theta_2}A_1, \quad \kappa_2 = \frac{2}{\tau_2} \quad (10)
\]

Here, \(\omega_1\) is the resonance frequency of the stub resonator. \(j\) is the imaginary unit \((j^2 = -1)\). The decay time of internal loss in the stub resonator is \(\tau_0\). \(\tau_1\) and \(\tau_2\) are the decay time from the stub to coupling waveguide and coupling cavity. \(\kappa_1\) is the coupling coefficient between the stub resonator and MIM waveguide, and \(\kappa_2\) is the coupling coefficient between the stub resonator and the composite cavity. \(\theta_i (i = 1, 2)\) is the phase of the coupling coefficient. \(\varphi\) and \(\delta\) are the phase change and amplitude attenuation between input and output SPPs waves of the stub resonator.
According to equations (7)-(10), the transmission $T$ of the proposed system above can be worked out and expressed as:

$$
T(\omega) = \left| \frac{S_{12} - S_{11}}{S_{11} + S_{12}} \right|^2 = \frac{\left| j(\omega - \omega_1) + \frac{1}{\tau_0} + \frac{1}{\tau_2} (1 - \delta e^{i\varphi}) / (1 + \delta e^{i\varphi}) \right|^2}{\left| j(\omega - \omega_1) + \frac{1}{\tau_0} + \frac{1}{\tau_1} + \frac{1}{\tau_2} (1 - \delta e^{i\varphi}) / (1 + \delta e^{i\varphi}) \right|^2}
$$

(11)

Here, the phase term $\varphi$ can be described as [61]:

$$
\varphi(\omega) = \frac{\omega_n L}{c} + \theta
$$

(12)

where, $\theta$ is the additional phase shift of the stub waveguide, $c$ is the speed of light in vacuum. In order to prove the accuracy of the research results in theory, we use the equation (11) to fit the simulation results based on CMT theory. The red dotted line in figure 2 is the fitting result, and the parameters of equation (11) are set as $\omega_1 = 1.8095 \times 10^{15}$ rad/s, $\tau_0 = 64.3824$ fs, $\tau_1 = 2.1310$ fs, $\tau_2 = 12.8279$ fs, $\delta = 0.9718$, $\theta = 0.05\pi$. Obviously, the fitting result is in good agreement with the simulation result.

To study the formation mechanism of Fano resonance, figure 3(a) shows the transmission spectra of the MIM waveguide with the stub resonator and with the ring cavity and the basic system. From this figure, it is found that the stub MIM waveguide shows a broadband transmission spectrum (the black dash dot line) called Lorentzian-like resonance marked as LR, whereas the ring cavity exhibits a narrow discrete spectrum (the blue dash line). Evidently, two sharp asymmetric transmission peaks are generated respectively near the corresponding positions of the two transmission valleys on the blue curve in figure 3 (a). Therefore, the formation of the FR and EIT can be explained by the interaction of the narrow discrete resonances (dark modes) of the ring cavity and the broad continuum resonance (bright mode) of the stub resonator. The asymmetric profiles FR and EIT originate from the reverse coherence properties...
(destructive or constructive) near the opposite sides of the resonant wavelength [18], [41], [42].

In order to further comprehend the underlying physics of these Fano resonances in the proposed system, the corresponding field intensity $|H_{z}|^2$ distributions at $\lambda = 680$ nm (FR peak) and 989 nm (EIT peak) are shown in figure 3 (b)-(c). Obviously, nearly all the energy is trapped in the ring resonator, separately exciting the standing wave pattern with $N = 6$ and $N = 4$. These high-order resonant modes are the dark modes with a narrowband response spectrum supported by the ring cavity. However, the bright mode with a broadband transmission spectrum is supported by the stub resonator. Therefore, the dark modes interfere with the bright mode, generating the FR and EIT line-shape. Based on equations (4)-(6), the incident wavelength $\lambda = 680$ nm (FR peak) / 989 nm (EIT peak) corresponds to the effective SPPs wavelength of $\lambda_{sp} = \frac{2\pi}{n_{eff}} = 485$ nm / 716 nm, so $N = \frac{2\pi}{2n_{eff}\lambda_{sp}} = \frac{2\pi}{2n_{eff}\lambda_{sp}} = 5.83 \approx 6/3.95 \approx 4$, which is consistent with the result of the numerical calculation in figure 3(b)-(c). Thus, we can make a simple inference that the resonant wavelengths of FR and EIT, respectively.

Compared with figure 3(d), the wavelengths of rapid phase shift change in figure 3(d) coincide well with the resonant wavelengths of FR and EIT, respectively.

As illustrated in figure 3(e), without ring cavity, there is anti-phase between the stub resonator and MIM waveguide at the wavelength of 971 nm. And the SPPs are coupled to the stub cavity. Then, they are completely reflected from the top of the stub cavity to form a strong standing wave pattern, which inhibits SPPs from continuing to transmit to the output of the waveguide and forms a transmission valley. By observing figure 3(f), it is obvious that the $H_{z}$ fields are anti-phase between the stub resonator and MIM waveguide, which induces destructive interference between the incident light and the light escaping into the MIM waveguide from the stub resonator and transmission suppression.

Nevertheless, the $H_{z}$ fields shown in figure 3(g) indicate that an in-phase relationship is noticeable between the stub resonator and MIM waveguide, which causes constructive interference between the two excitation pathways and transmission enhancement. Therefore, the power flow is confined to the stub and ring cavity, and the dark mode from the ring cavity interferes with the bright mode from stub resonator, resulting in FR. From the $H_{z}$ field distributions at $\lambda = 955$ nm and $\lambda = 1088$ nm which are shown in figure 3(h) and (j), it can be observed that there are anti-phase between the stub resonator and input MIM waveguide, namely the condition of resonance destructive is met, giving rise to the destructive interference between the two optical paths and transmission suppression. Whereas for $\lambda = 989$ nm (the EIT peak), which is shown in figure 3(i), the $H_{z}$ fields in the poorly coupled stub resonator are in-phase with the $H_{z}$ fields in input MIM waveguide, which causes the coherence enhancement to generate the EIT-like phenomenon [47], [51]. Therefore, the dark mode supported by the ring cavity interferes with the bright mode from stub resonator, leading to EIT. As shown in figure 3(j), a strong magnetic field emerges in the stub resonator, whereas extremely weak magnetic field appears in the ring resonator. It indicates that the SPPs do not resonate in the ring cavity because the incident wavelength ($\lambda = 1088$ nm) is far from the resonant wavelength ($\lambda = 955$ nm) of the ring cavity.

### III. MULTIPLE FANO AND EIT-LIKE RESONANCES INDUCED BY CONNECTING AN INNER RING CAVITY TO THE RING RESONATOR THROUGH A SLOT

The basic proposed structure above is well malleable and can be easily extended to a quadruple Fano resonances and double EIT-like responses system by connecting an inner ring cavity to the ring resonator through a slot and adding a ring cavity under the stub.

### IV. TRIPLE FANO RESONANCES INDUCED BY CONNECTING AN INNER RING CAVITY TO THE RING RESONATOR THROUGH A SLOT

To further research the basic structure discussed above, an inner ring cavity is connected to the ring resonator by a slot, which is plotted in figure 4(a). Herein, the length of the slot is $k = 60$ nm, and the center of the inner disk is $O_{2}$. The radius of the inner ring is $R_{0} = 130$ nm, and the width of the inner ring is fixed as $w = 50$ nm. Besides, other parameters are the same as the structure in section II. In figure 4(b), comparing with the transmission spectrum of the basic structure, it can be observed that the resonant wavelengths of FR and EIT are slightly moved, and two new Fano resonance line-shapes arise due to the structural breaking [33], [34], [62], marked as NFR1 and NFR2. This is because the symmetry of the basic structure is broken after the introduction of the end-coupled cavity. According to the reference [62], new higher-order resonant modes (dark modes) will be generated, which interfere with the bright mode generated by the stub cavity to produce new Fano resonances. At the same time, based on equation (5), the resonant wavelength is proportional to the length of the resonator, and inversely proportional to the order of the resonant mode. Nevertheless, the change caused by the increase of the length of the resonant and the increase of the resonant order which is caused by the structural breaking do not cancel each other out, so the resonant wavelengths of FR and EIT are slightly moved. Next, we can still change the resonant wavelength of the derived structure by adjusting the length of the cavity. To investigate the formation mechanisms of the Fano resonances in the derived structure, the phase shift spectrum of the derivative structure and the field intensity $|H_{z}|^2$ distributions at $\lambda = 650$ nm (FR peak), 795 nm (NFR1 peak), 973 nm (EIT peak), and 1560 nm...
(NFR2 peak) are displayed in figure 4(c)-(g), respectively. In comparison with figure 4(b), the wavelengths of rapid phase shift change in figure 4(c) are coincident with the resonant wavelengths of FR, NFR1, EIT and NFR2, respectively. As shown in figure 4(d), almost all the energy is limited in the ring resonator to excite a narrow high-order resonant mode (dark mode). And the dark mode interferes with the broad low-order resonant mode (bright mode) resulting from stub resonator to produce FR, which indicates that FR is mainly influenced by the ring mode, namely the resonant wavelengths of FR is redshifted with the length of the ring cavity increasing. Similarly, it is noticed that almost all the energy is confined in the inner ring cavity, which indicates that the inner ring cavity is coupled with the ring cavity and produces a new narrow high-order mode termed as inner ring mode from figure 4(e). Namely, NFR1 is mainly produced by inner ring mode. Whereas EIT and NFR2 are mainly affected by the ring-inner ring mode according to figure 4(f) and (g). In this system, the inner ring mode and the ring-inner ring mode are dark modes, and they are coupled with the bright mode form stub to result in NFR1, EIT and NFR2. Therefore, we can tune these Fano resonances by changing the structural parameters.

To further test the analysis above, the transmission spectra of the derived structure are studied by altering the structural parameters. According to equation (5), the resonant wavelength has linear redshift as the length of the resonator increases. When the length of the slot $k$ increases from 20 nm to 80 nm with a step of 20 nm with other parameters kept constant, the resonant wavelengths are nearly linear redshifted, which is displayed in figure 5(a). To further verify this linear dependence, the resonant wavelengths of FR, NFR1, EIT and NFR2 are calculated, and the results do exhibit this linear characteristic, which are illustrated in figure 5(b). In addition, the influence of $R_0$, which alters from 110 nm to 140 nm with a step of 10 nm, on the transmission spectra is investigated, and the results are shown in figure 5(c). It is obvious that FR resonance peak is slightly moved, affirming that FR is mainly induced by the ring mode, and it is also affected by the inner ring mode to a small degree. Thus they will be slightly influenced by variable $R_0$, which is identical to the results of previous analysis. And the resonant wavelengths of EIT and NFR2 have an evident redshift on account of the fact that EIT and NFR2 are mainly influenced by the ring-inner ring mode. Evidently, the NFR1 have a more drastic redshift because it primarily originates from the inner ring mode. In a similar way, the resonant wavelengths of FR, NFR1, EIT and NFR2 are calculated, which are shown in figure 5(d). Through the adjustment of the structural parameters, the derived system can be better tuned and controlled.
FIGURE 5. (a) The transmission spectra of the derived structure with changing from 20 nm to 80 nm. (b) The resonant wavelengths of FR, NFR, EIT and NFR2 with different k. (c) The transmission spectra of the derived structure with varying R0 from 110nm to 140nm. (d) The resonant wavelengths of FR, NFR, EIT and NFR2 with different R0.

V. QUADRUPLE FANO RESONANCES AND TRIPLE EIT-LIKE RESPONSES BY INTRODUCING ANOTHER RING CAVITY

To further improve the sensing performance of the system in section III.A and provide more sensing check-points and even to design multi-spectrum sensor, another ring cavity is added under the stub MIM waveguide with the distance g of 10 nm, as shown in figure 6(a). The thickness of the lower ring cavity is also set as w = 50 nm, and the radius R1 = 250 nm. The transmission spectra of the system in Section III.A and III.B are shown in figure 6(b). It should be observed that the resonant wavelengths of FR, NFR1, EIT, and NFR2 basically remain unchanged. Besides, two new Fano resonance line-shapes arise, marked as NFR3 and NEIT. In comparison with figure 6(b), the wavelengths of rapid phase shift change in figure 6(c) are coincident with the resonant wavelengths of FR, NFR3, NFR1, EIT, NEIT, and NFR2, respectively. To further explore the origin of quadruple Fano resonances and double EIT-like effects, the field intensity (|Hz|^2) distribution at the peak of FR (λ = 648 nm), NFR3 (λ = 703 nm), NFR1 (λ = 796 nm), EIT (λ = 971 nm), NEIT (λ = 1009 nm), NFR2 (λ = 1561 nm) are displayed in figure 6 (d)-(i), respectively. The |Hz|^2 distributions at FR, NFR1, EIT, and NFR2 are nearly identical to those in figure 4 (d)-(g), which indicates that FR is still largely influenced by ring mode, NFR1 is still mainly caused by inner ring mode, EIT and NFR2 are mainly induced by ring-inner ring mode based on the discussion in section III.A. Nevertheless, compared with figure 4(d) and (f), a small portion of the energy in figure 6 (d) and (g) is restricted in the lower ring, resulting in a lower transmittance of the system in section III.B than that in section III.A. In figure 6 (e) and (h), the SPPs are confined in the lower ring cavity at λ = 648 nm (NFR3) and λ = 703 nm (NEIT), exciting a new high-order mode (dark mode) termed as lower ring mode. The NFR3 and NEIT originate from the interference between the lower ring mode and the low-order resonant mode (bright mode) from the stub.

VI. POTENTIAL APPLICATIONS OF THE PROPOSED MULTIPLE FANO AND EIT-LIKE RESONANCES STRUCTURES

A. SENSING POTENTIAL OF THE STRUCTURES

The sensing performance of our structures above is illustrated with its response for different refractive indices of the white etches in figure 4(a) and 6(a). The structural parameters are those used in figure 4(a) and 6(a), and the refractive index n varies from 1.00 to 1.03 at interval of 0.01.
The sensing performance of the derived structure in section III.A is displayed in figure 7(a), which shows that these triple Fano resonances and single EIT-like response have a redshift when $n$ increases from 1.00 to 1.03. The sensitivity ($S$) of the refractive index sensor can be defined as the shift in the resonance wavelength per unit change of the refractive index, as defined as $S = d\lambda/dn$ (nm/RIU) [6]. Thus, the $S$ are 600 nm/RIU, 800 nm/RIU, 1000 nm/RIU, and 1600 nm/RIU at FR, NFR1, EIT, and NFR2, respectively, which can be obtained from figure 7(b).

The FOM is another crucial and more illustrative parameter to evaluate the sensing performance of the system, expressed as $FOM = \Delta T/T \Delta n$ [20], where $T$ is the transmittance of the system and $\Delta T/\Delta n$ denotes the transmittance variation at the constant wavelength induced by the alteration of $n$. As can be seen from figure 7(c), the FOMs are calculated for the refractive indexes 1.01, 1.02, and 1.03 as $FOM = (T_{n=1.01}/T_{n=1.02}/T_{n=1.03} - T_{n=1})/(T_{n=1} \Delta n)$, among which the maximum can reach 2685 at 949 nm, which is larger than that in the previous report about refractive index sensors [40], [50], [53].
Similarly, we further explore the sensing potential of the derived system in section III.B, which is displayed in figure 8(a), (b) and (c). Herein, the proposed structure still has great sensitivity, about 600 nm/RIU, 700 nm/RIU, 800 nm/RIU, 1000 nm/RIU, 1000 nm/RIU, 1600 nm/RIU at FR, NFR3, NFR1, EIT, NEIT, and NFR2, respectively.
As shown in figure 8(c), though these FOM lines are different in the maximal values, it is noteworthy that the maximum FOM can reach the order of $10^6$ in the case of EIT, which is remarkably higher than the vast majority of proposed refractive index nanosensors [6], [18]–[21], [40]–[45], [53], [55], [63], [65]–[67].

B. SLOW LIGHT EFFECTS OF THE MULTIPLE FANO AND EIT-LIKE RESONANCES

Analogous to conventional EIT in atomic systems, the proposed EIT-like resonator above can also induce rapid phase changing and support slow group velocities, which is needed by the slow light applications. The slow light effects can be assessed by the group delay time $\tau_g$ (ps) and the group index $n_g$, which are expressed as [54], [56]

$$\tau_g = \frac{d \psi (\omega)}{d \omega} = -\frac{\lambda^2}{2\pi c} \frac{d \psi (\lambda)}{d \lambda}$$  \hspace{1cm} (13)
$$n_g = \frac{c}{v_g} = \frac{c}{D \tau_g} = -\frac{\lambda^2}{2\pi D} \frac{d \psi (\lambda)}{d \lambda}$$  \hspace{1cm} (14)

where $\psi (\lambda)$ and $c$ are transmission phase shift and the speed of light in vacuum, respectively, $v_g$ is the group velocity of the EIT-like structure and $D = 2$ um is the length from the incident light to the output port. According to equations (13), (14) and figure 4(c), the $\tau_g$ (ps) and $n_g$ are numerically calculated, which are shown in figure 9 (a) and (b). It can be seen that the maximum delay time and group index are about 0.25 ps and 37 at around NEIT, which are around five times of those of the Fano system [57].

In the same way, figure 10 (a) and (b) represent the $\tau_g$ (ps) and $n_g$. Obviously, there are large group delays and indexes around the Fano and EIT-like resonances, among which the maximum delay time and group index are about 1.49 ps and 221 at around EIT, which are around six times of those of the system presented in section III.A.

C. SWITCHING APPLICATIONS OF THE SYSTEM

Optical switch is essential for the next generation of highly integrated optical circuits [54], [58]. The steep Fano and EIT-like line shapes proposed in this literature are ideal for...
TABLE 1. Comparison of the proposed structure and the latest relevant structures.

| Reference | Type | S       | FOM       | $\tau_g$ | $\eta_g$ | EXT |
|-----------|------|---------|-----------|----------|----------|-----|
| [6]       | 4    | 500/850/950/1300 | Max 4.038x10^4 | N/A      | N/A      | N/A |
| [7]       | 1    | 1280    | N/A       | N/A      | N/A      | 30dB|
| [18]      | 4    | 680/820/840/1100 | Max 3.2x10^4 | N/A      | N/A      | N/A |
| [19]      | 1    | 1400    | 2.3x10^4  | N/A      | N/A      | N/A |
| [20]      | 4    | 800/1300/2000 | Max 4.05x10^4 | 0.61ps   | N/A      | N/A |
| [21]      | 4    | 650/900/1350/2000 | Max 4452 | 1.17ps   | N/A      | N/A |
| [22]      | 3    | 760/1320/1640 | Max 3.7x10^4 | N/A      | N/A      | N/A |
| [23]      | 1    | 1057    | N/A       | N/A      | 695      | N/A |
| [40]      | 1    | 733     | N/A       | N/A      | 695      | N/A |
| [41]      | 4    | 650/750/1100/950 | Max 2.73x10^4 | N/A      | N/A      | N/A |
| [42]      | 4    | 800/1000/1600/1900 | Max 3.8x10^4 | N/A      | N/A      | N/A |
| [43]      | 2    | 850/1120 | Max 1.7x10^4 | N/A      | N/A      | N/A |
| [44]      | 4    | 416/520/866/986 | Max 3.2x10^4 | N/A      | N/A      | N/A |
| [45]      | 2    | 1350/800 | Max 3.51x10^4 | N/A      | N/A      | 91dB|
| [53]      | 2    | 1040/980 | 198.9/197.6 | N/A      | N/A      | N/A |
| [54]      | 1    | N/A     | N/A       | N/A      | 26       | N/A |
| [55]      | 1    | 1277    | 2.2x10^4  | N/A      | 180      | N/A |
| [56]      | 1    | N/A     | N/A       | N/A      | 51       | N/A |
| [57]      | 1    | 800     | N/A       | 0.053ps  | N/A      | N/A |
| [59]      | N/A  | N/A     | N/A       | N/A      | 16.6dB,10.37dB |
| [60]      | N/A  | N/A     | N/A       | N/A      | 32.1dB   |
| [64]      | 1    | 903     | Max 4.6x10^4 | N/A      | N/A      | N/A |
| [65]      | 1    | 1260    | Max 2.3x10^4 | N/A      | N/A      | N/A |
| [66]      | 1    | 718     | Max 4354  | N/A      | N/A      | N/A |
| [67]      | 3 to 7 | Max 1382 | Max 48.6dB (10^-49) | 0.14ps  | N/A      | N/A |

| This work | 6    | 600/700/800/1000/1000/1600 | Max 1.2x10^6 | 1.49ps   | 221      | 43dB |

devising all-optical switches. As shown in figure 6(b), the transmittance of the proposed structure can sharply drop from EIT peak (“on state”) to EIT dip (“off state”) with wavelength shifts about 17 nm, and thus this characteristic can be used for designing an all-optical switch. The on/off extinction ratio is a key indicator to evaluate the performance of the optical switch, which is expressed as [59]

$$EXT = 10 \log \frac{T_{\text{max}}}{T_{\text{min}}} \text{ (dB)}$$ (15)

where $T_{\text{max}}$ and $T_{\text{min}}$ represent the transmission of the peak (“on state”) and dip (“off state”), separately. According to the formula above, the extinction ratio at EIT is about 43 dB, which is greater than the previous researches [7], [59], [60]. This work lays the groundwork for the design of high-performance optical switches with fast response combined with Kerr materials in the future. [63], [68]

Finally, in order to clearly illustrate the advantages of the proposed structure in various applications, the table 1 is made, which compares the performance parameters of our structure with those of other similar structures and systems which can produce multiple Fano or EIT-like resonances published in recent years. In this table, type represents the number of Fano or EIT-like profiles of a system. From the table we can draw the conclusion that our structure has relatively good sensitivity and it is superior to other structures in both the maximal FOM and the number of Fano or EIT-like resonances [6], [18]–[21], [40]–[45], [53], [55], [64]–[67]. Besides, the slow light effects of our system outperform other researches in the reference [20], [54]–[57], which shows great promises for highly integrated slow light applications. And it is worth mentioning that the extinction ratio of the proposed system is higher than that of most other proposed structures in the reference [7], [59], [60]. All in all, the proposed structure can play a significant role in highly integrated plasmonic devices including refractive index sensors, slow light devices, optical switches.

VII. CONCLUSION

In summary, Fano resonance and EIT-like effect in the basic proposed structure are numerically calculated. Based on this, an inner ring is introduced to create a new coupled plasmonic structure, which provides triple Fano resonances and single EIT-like profile and yields an ideal sensitivity of 1600 nm/RIU but the maximal FOM value of 2685 is not high enough. Besides, its maximum group delay time and group index are about 0.25 ps and 37. Such properties are greatly improved by adding another ring cavity under the stub MIM waveguide to create a new coupled plasmonic structure as well, providing quadruple Fano resonances and double EIT-like effects and yielding a great sensitivity of 1600 nm/RIU and the ultra-high maximal FOM.
value of $1.2 \times 10^6$, which is better than the vast majority of researches up to the present. Moreover, a maximum group delay time and group index about 1.49 ps and 221 at around EIT can be realized, which is quite promising for on-chip slow light applications. Finally, an all-optical switch is also studied based on the EIT-like resonance with an on/off contrast ratio about 43 dB. It is believed that the proposed structures can support substantial excellent applications such as bio-chemical nanosensors, slow light and nonlinear devices, optical switches and filters in highly integrated plasmonic devices.

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