Status and Prospects of Discrete Symmetries Tests in Positronium Decays with the J-PET Detector

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Abstract. Positronium is a unique laboratory to study fundamental symmetries in the Standard Model, reflection in space (P), reversal in time (T), charge conjugation (C) and their combinations. The experimental limits on the C, CP and CPT symmetries violation in the decays of positronium are still several orders of magnitude higher than the expectations. The newly constructed Jagiellonian Positron Emission Tomograph (J-PET) was optimized for the registration of photons from the electron-positron annihilations. It enables tests of discrete symmetries in decays of positronium atoms via the determination of the expectation values of the discrete-symmetries-odd operators. In this article we present the capabilities of the J-PET detector in improving the current precision of discrete symmetries tests and report on the progress of analysis data from the first data-taking runs.

INTRODUCTION

One of the greatest achievements of the twentieth century theoretical physics was a formulation and proof of Noether’s theorem which connects symmetries of physical systems and conservation laws [1]. Ever since then symmetries have become an essential toolbox of almost all physics theories and models, especially in particle physics. Every quantum field theory describing the interaction and properties of elementary particles is formulated requiring Lorentz invariance. An important role in the Standard Model formulation has been played by the discrete symmetries of Parity P, Charge Conjugation C and Time Reversal T and their combinations, CP and CPT. They prove to be very useful in the calculation of the cross sections and decay rates, especially for the processes governed by the strong interaction [2]. Among all the known forces only the weak interaction leads to phenomena violating the invariance under the three discrete operations and their combination, CP. The P invariance violation was first observed in the β decay of 60Co isotope [3], while soon after this discovery it was shown that the P and C symmetries are violated in the subsequent decays of charged pions and muons [4]. The time reversal symmetry breaking have been observed far only by the CPLEAR Collaboration in neutral kaons transitions of CP-conjugate states [5] and by the BaBar Collaboration in B mesons decays using transitions between their pure flavour and CP-definite states [6]. Currently analogous test have been performed for neutral kaons by the KLOE-2 Collaboration [7–9]. The combined symmetry CP operation was thought to be exact until the regeneration studies of the neutral K mesons by Christenson, Cronin, Fitch and Turlay [10]. In the Standard Model the CP violation mechanism is introduced by the quark mixing described by the complex Cabibbo-Kobayashi-Maskawa matrix with one nonzero phase [11, 12], which explicitly requires existence of the three generations of quarks [2]. The CP violation in the kaon sector is well known due to several experiments, mainly the NA48 [13], KTEV [14] and KLOE [15], but there are still several open issues under investigation mainly related to rare and ultra rare kaon decays. The CP-violating K_1 \to \pi^0 \nu \nu and K^+ \to \pi^+ \nu \nu decays have been searched recently by the KOTO [16] and NA62 [17] experiments. The CP violation is also still not well measured for the K_2 meson, especially in the three-pion and semileptonic decays [18, 19]. In the B meson decays the violation of this symmetry appears to be even stronger than for K mesons [20]. As in case of kaons it was found in the mixing of B^0 \to \bar{B}^0 [21, 22] and directly in the decay amplitudes of B^0 [23, 24], B^+ [25–27] and B_q^0 [28].

The CP symmetry is very important in view of the observed matter-antimatter asymmetry which requires much larger violation than predicted by the Standard Model. Therefore, a lot of effort is made nowadays to find a new sources of CP and C symmetries breaking. Apart from the D meson decay studies [20] discrete symmetries violation is searched
in baryonic systems [29] and in the leptonic sector, in particular in the positronium decays [30–32] and in neutrino oscillations [33]. Invariance under the \( CP \) operator is also of a great importance since its violation would be an unambiguous sign of phenomena not included in the Standard Model. There have been performed many tests, including neutral kaons [19, 34–37], \( B \) meson system [38] and positronium decays [39], and so far this symmetry seems to be exact for all the known interactions.

**POSITRONIUM AS A PROBE FOR DISCRETE SYMMETRIES TESTS**

In the leptonic sector positronium is a very promising system to test discrete symmetries and to look for physics beyond Standard Model. It is a simple bound state of an electron and a positron which formation and decay is governed by QED. Positronium is an eigenstate of the \( P \) operator, as a system bound by a central potential, and \( C \) as well (particle-antiparticle state). In the ground state the parity of positronium is equal to \( \lambda_p = -1 \), while the charge conjugation eigenvalue depends on spin \( S \) of the system: \( \lambda_C = (-1)^S \). Thus, para-positronium \((S = 0)\) is a \( CP \)-odd state and the spin-triplet state, ortho-positronium, is even with respect to this operator. Since QED is invariant under all the mentioned operations discovery of violation of any discrete symmetries would be a sign of some new processes not described by the Standard Model. In case of positronium these tests can be made with a very high precision. For example, the expected \( CP \) violation effects in the ortho-positronium \((o-Ps)\) decays are expected to be at the level of \( 10^{-10} \) due to the photon-photon interactions [40]. The tests of invariance under a certain operation may be conducted directly, by searching for transitions leading to final state with opposite eigenvalue than the initial one. With positronium one can test this in way for example the \( C \) symmetry by searching for \( o-Ps \) and \( p-Ps \) decays to an even and odd number of photons, respectively. Experiments done so far led to the following upper limits on branching ratios for \( CP \) violation effects in the ortho-positronium \((o-Ps)\) decays are expected to be at the level of \( 10^{-10} \) due to the photon-photon interactions [40]. The tests of invariance under a certain operation may be conducted directly, by searching for transitions leading to final state with opposite eigenvalue than the initial one. With positronium one can test this in way for example the \( C \) symmetry by searching for \( o-Ps \) and \( p-Ps \) decays to an even and odd number of photons, respectively. Experiments done so far led to the following upper limits on branching ratios for both spin states: \( BR (o-Ps \rightarrow 4\gamma/o-Ps \rightarrow 3\gamma) < 2.6 \cdot 10^{-6} \) at 90% C. L. [41], \( BR (p-Ps \rightarrow 3\gamma/p-Ps \rightarrow 2\gamma) < 2.8 \cdot 10^{-6} \) at 68% C. L. [42], \( BR (p-Ps \rightarrow 5\gamma/p-Ps \rightarrow 2\gamma) < 2.7 \cdot 10^{-7} \) at 90% C. L. [43]. The alternative way of testing are measurements of non-vanishing expectation values of certain operators odd under the transformation [44]. For \( o-Ps \rightarrow 3\gamma \) they can be constructed from momenta of the final-state photons, their polarization and spin of the positronium [31]. Some of the operators of interest are listed in Tab. 1. The \( k_1, k_2, k_3 \) denote momenta of the three photons in ascending order according to their moduli [31] and \( \epsilon_1, \epsilon_2 \) and \( \epsilon_3 \) are their polarization vectors, respectively. The quantization axis of the spin of \( o-Ps \) requires a static magnetic field, which mixes the two positronium spin states for the spin projection \( j_z = 0 \). This shortens effectively the ortho-positronium lifetime and allows one to determine the spin polarization. For elemental positrons one can determine the spin direction taking advantage that due to the parity violation the positrons are linearly polarized along their velocity direction. This polarization is preserved to high extend during the positronium formation [31, 45]. Up to now the experiments were performed only for the \( CP \) and \( CP^{'} \) symmetries yielding the following mean values of corresponding operators: \( \left\langle \vec{S} \cdot k_1 \left[ \vec{S} \cdot (k_1 \times k_2) \right] \right\rangle = 0.0013 \pm 0.0012 \) [32] and \( \left\langle \vec{S} \cdot (k_1 \times k_2) \right\rangle = 0.0071 \pm 0.0062 \) [39].

**PROSPECTS OF DISCRETE SYMMETRIES TESTS WITH THE J-PET DETECTOR**

One of the ongoing experiments having potential to significantly improve the sensitivity of the discrete symmetries is the J-PET experiment [30, 31, 46–48]. Designed as novel cost-effective and full-body PET scanner [49–51], the J-PET detector constitutes a multipurpose device for fundamental particle physics studies [31, 52, 53]. In its current configuration it consists of 192 detection modules made out of long EJ-230 scintillator bars with dimensions 19x7x500 mm$^3$ arranged in three layers. Light produced by gamma quanta interaction in each scintillator is collected by Hamamatsu R9800 photomultipliers connected optically to both ends of the strip. The J-PET detection setup is

| Operators | Tested Symmetries |
|-----------|-------------------|
| \( \vec{S} \cdot k_1 \) | \( \vec{S} \cdot (k_1 \times k_2) \) | \( CP, CP', CP^{'} \) |
| \( \vec{S} \cdot (k_1 \times k_2) \) | \( \vec{S} \cdot \epsilon_1 \) | \( T, CP^{'} \) |
| \( \vec{S} \cdot (\vec{S} \cdot k_1) \) | \( \vec{S} \cdot (k_1 \times k_2) \) | \( CP, T, CP^{'} \) |
They can be separated using the time difference from the corresponding ortho-positronium one can take advantage of the completely different lifetimes of the two spin states. They differ in different lifetimes of the two spin states. The three photons originating from the ortho-positronium decay are detected with an efficiency of about \(10^{-4}\). The J-PET detector has been successfully commissioned and have been taking data with several different vacuum chambers and targets for ortho-positronium formation [61, 62]. The preliminary analysis of gathered data revealed that the main background for the ortho-positronium decay studies is composed by the pick-off annihilations or ortho-para spin conversion due to the spin-orbit interaction or due to electron exchange [31]. These processes lead to the final state with two 511 keV photons which may scatter and mimic the ortho-positronium decay studies with the J-PET detector [31]. An open Na source is placed inside a vacuum chamber (red circle) in the geometric center of the J-PET detector. Positron originating from the beta decay may form ortho-positronium in a porous material placed on the inner surface of the chamber (black dot). The three gamma quanta from ortho-positronium decay, with momenta \(k_1, k_2, k_3\), are registered by the J-PET detector. The measurement of ortho-positronium lifetime is provided by the registration of the gamma quantum from the deexcitation of the \(^{22}\)Ne isotope originating from the sodium beta decay. Figure adapted from [60].

Photomultipliers signals are probed at four thresholds on both, leading and trailing edges by novel front-end electronics with accuracy of about 30 ps [54]. It provides also signal’s charge determination by the Time-Over-Threshold (TOT) measurement, which leads to the determination of the gamma quanta energy loss with accuracy of about \(\sigma(E)/E = 0.044/E(\text{MeV})\) [46]. The J-PET FPGA-based data acquisition system is working in a continuous readout mode and allow true real-time tomographic data processing [55, 56]. The J-PET time resolution of annihilation gamma quanta registration amounts to about \(\tau \sim 125\) ps [46] and will be further improved by using dedicated reconstruction methods taking advantage of signals probing at the four thresholds [47, 57, 58]. Using the J-PET detector one can test the discrete symmetries both, by searching for forbidden decays and by measurement of asymmetry-odd operator expectation values. As it was shown in Fig. 1b) the measurements have been done with a \(^{22}\)Na positron source, enclosed in a thin kapton foil to minimize annihilations in the source itself, placed in an vacuum chamber covered with a material maximizing the formation of ortho-positronium with a long lifetime [59]. As it was mentioned in the previous section the positron is linearly polarized along its velocity and there is a high probability that the spin direction does not change during the ortho-positronium formation. Thus, to determine the ortho-positronium spin direction one can measure the positron velocity direction. This can be done by reconstructing the position of the positronium formation by a dedicated trilateration method [48]. The ortho-positronium lifetime measurement is done using a gamma quantum from excited \(^{22}\)Ne associated to the positron emission. It can be distinguished from the annihilation and scattered photons via the TOT measurement which is much higher for deexcitation quanta. The three photons originating from the ortho-positronium decay are detected with an efficiency of about \(10^{-5}\) depending on the energy loss threshold used [30]. The plastic scintillators used in the J-PET detector enable also determination for the gamma quanta polarization. Since the most probable effect of annihilation gamma quanta interaction is the Compton scattering occurring most likely in the plane perpendicular to the electric vector of the photon, measurement of four-momenta of annihilation and corresponding scattered quanta allows to determine, to some extent, linear polarization of the primary quanta, e.g. by the following cross product: \(\vec{\varepsilon}_\gamma = \vec{k} \times \vec{k}'\), where \(\vec{k}\) and \(\vec{k}'\) are the momenta of the annihilation and scattered photon [31]. The J-PET detector have been successfully commissioned and have been taking data with several different vacuum chambers and targets for ortho-positronium formation [61, 62].
FIGURE 2. a) Distribution of the difference of two smallest relative angles between reconstructed momenta of photons in a function of their sum obtained with a small sub-sample of the J-PET data. The $\omega$-$Ps \rightarrow 3\gamma$ signal region is showed as a black triangle; b) Lifetime spectrum of positronium registered with the J-PET detectors.

citation gamma quantum. An exemplary distribution of such difference measured with the J-PET detector is shown in Fig. 2b). Such distributions can be used also in the Positron Annihilation Lifetime measurements which may be used in medical diagnostics [63, 64].

SUMMARY

Discrete symmetries have been playing an exceptional role in formulation and tests of the Standard Model. Violation of the $P$, $C$ and $CP$ symmetries by the weak interactions is well established for neutral kaons and $B$ mesons, while there is still no experimental evidence of analogous breaking in the baryonic or leptonic sectors. As the lightest purely charged leptonic state, positronium constitutes one of the best systems to search for new effects not included in the Standard Model. In this case the symmetries can be tested by searching for the forbidden decays, e.g. $p$-$Ps \rightarrow 3\gamma$, or by measurement of expectation values of symmetry-odd operators. One of the experiments which has a great potential in providing new experimental data in this sector is the J-PET detector since it has a unique capability of positronium spin determination and gamma quanta polarization [65]. With the present detector and near future upgrades [50, 66–68] J-PET will be able to test discrete symmetries in the charged lepton system with significantly higher sensitivity than presently published results.

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