Spin-glass transition in porous spheres BiFeO$_3$

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Magnetic properties of porous spheres BiFeO$_3$ have been studied at temperatures ranging from 2 to 300 K. A transition to cluster spin glass state has been detected in the region of about 100 K. The presence of the transition is confirmed by nonlinear variation of coercive force and the appearance of exchange displacement of magnetic hysteresis loops at temperature below 100 K. Temperature dependence of magnetization for zero-field cooled regime exhibit a maximum at some temperature $T_m$. The function $T_m(H)$ ($H$ is magnetic field) changes in accordance with Almeida–Thouless line.

The performed measurements of the frequency dependence of AC susceptibility confirm the behavior of spin glass with spin freezing temperature $T_f = 116$ K. The critical index $z\nu = 2.5$ agrees well with the mean-field theory $z\nu = 2.0$.

**Keywords:** bismuth ferrite, magnetic properties, porous spheres, Almeida–Thouless line, spin cluster glass.

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1. Introduction

It is known that the bismuth ferrite BiFeO$_3$ (BFO) is one of few materials exhibiting multiferroic properties at room temperature. However, bulk BFO is not suitable for application because of a spin cycloid with period length of 62 nm in its magnetic structure [1] that reduces weak ferromagnetism to zero, thus preventing the appearance of a linear magnetoelectric effect [2]. Reduction to nanodimensionis an effective method of ferromagnetic order formation in BFO system due to an increase of the fraction of uncompensated spins and suppression of spiral order as a result of reduction of crystallite sizes [3, 4]. Both in thin BFO films and nanocrystals, magnetic switching can be induced by electric field [5,6], which opens up prospects for practical application of BFO in magnetic sensors, spintronics and data storage devices [1].

Recently, the study of magnetic properties was focused on BFO films and nanopowders. Different experiments, including direct magnetic measurements, suggest several magnetic transitions in the temperature range from 5 to 250 K [7–9]. The nature of these transitions is not entirely understood. They can be related either to spin orientation variation or to transition to spin glass state. The results of neutron diffraction studies and investigations of Raman spectra and dielectric properties revealed the presence of a phase transition connected with spin reorientation at 150 K [10–12]. Spin reorientation transition facilitates transition to spin glass state at further decrease of temperature [12]. The majority of researchers of nanocrystalline powders believe that magnetic properties can be explained in the model of antiferromagnetic nucleus with ferromagnetic shell. At the same time, some questions remain undetermined. Unusual effects of exchange displacement of hysteresis loop above transition temperature to spin glass state and nonmonotonic variation of coercive force require further research [9, 13]. Park et al. [3] inferred that the anomalous magnetization behavior in BFO nanoparticles arises from a complex interplay between the finite size effects, interparticle interaction, and a random distribution of anisotropy axis in nanoparticle assemblies. The systems of interacting magnetic nanoparticles may demonstrate a large variety of phenomena, which are of interest both for fundamental scientific studies and future practical applications of magnetic nanoparticles [14].

Examples of nanoparticles assembling are such materials as nanofibers [15], nanotubes [16], hollow spheres [17, 18] etc. consisting of randomly oriented nanocrystals [15, 18]. Earlier we showed that spherical agglomerates of about 1 $\mu$m in size possess at room temperature weak ferromagnetism typical of nanoparticles making up spheres [18]. At the same time, there are no available data on the presence of low-temperature phase transitions typical of nanoparticles. At present, almost no experimental studies of low-temperature magnetic properties of nanostructured BFO are available.

In this work, the magnetic properties of spherical porous BFO agglomerates produced by ultrasonic spray pyrolysis are comprehensively studied in the temperature range 2 – 300 K. Based on the results of field and temperature dependences of magnetization, magnetic AC susceptibility measurements we have established the existence of a phase transition to spin glass state in the examined materials.
2. Experimental

Spherical BFO agglomerates were synthesized by ultrasonic spray pyrolysis (USP) from a solution of iron and bismuth nitrates with addition of 6 moles of tartaric acid (TA) per 1 mole of BiFeO$_3$. The synthesis procedure is described in detail in works [18, 19].

X-ray powder diffraction (XRPD) analysis was carried out using an XRD-7000 (SHIMADZU) diffractometer with a secondary monochromator with Cu K$_{α}$ radiation in the 2θ range from 20 to 80° with a step of 0.03°. Structural investigations were performed in transmission geometry using an automatic STOE STADI-P diffractometer equipped with a linear mini-PSD detector using Cu K$_{α1}$ radiation in the 2θ range from 5 to 120° with a step of 0.02°. Polycrystalline silicon ($a = 5.43075(5)$ Å) was used as an external reference.

The morphology of the samples and 3D FIB-SEM tomography study were carried out using a TESCAN LYRA 3 dual beam system.

Magnetic measurements were carried out using setups of Quantum Design – MPMS-XL-7 (UFU) as well as PPMS-9 of the Collaborative Access Center “Testing Center of Nanotechnology and Advanced Materials” of the Institute of Metal Physics.

3. Results and discussion

The X-ray diffraction patterns of BFO sample are presented in Fig. 1(a). All the basic reflections correspond to ferrite BiFeO$_3$ with perovskite structure and space group R3c (ICSD Collection Code 15299). The lattice parameters are calculated by way of full-profile analysis of X-ray diffraction patterns with the use of structural models of the corresponding compounds ($a_{hex} = 5.58851$, $c_{hex} = 13.7852$). The sizes of coherent scattering regions (CSR) were found by the Le Bail method using the Klug & Alexander approach [20], allowing the contribution of size effects to FWHM to be determined. The value of CSR, calculated from the X-ray diffraction patterns, is proportional to the sizes of nanocrystallites composing the agglomerates (CSR = 26.2 nm). Therefore, hereafter, we shall consider that the CSR value is equal to nanocrystallite size. For the analysis of lattice distortions we used the rhombohedral cell parameters $a = a_{hex}/\sqrt{2}$ and $c = c_{hex}/2\sqrt{3}$ ($c/a = 1.0070$). The obtained nanocrystal sizes and the lattice distortion parameter coincide with the results of structural studies of nanopowders reported in work [21]. Earlier, we showed [18] that the samples synthesized by USP technology contain no oxygen vacancies, and all Fe ions have valence 3+.

The electron microscopy study of the powders reveals that all the samples produced from solutions with TA concentration 6 mol TA/mol BFO represent porous agglomerates of spherical shape. The mean diameter of the agglomerates determined from the results of 300 – 400 measurements amounted to about 1.2 microns (Fig. 1(b)). The internal structure of agglomerates was studied by the SEM method with focused gallium ion beam polishing (FIB). Fig. 1(c) displays a SEM image of an agglomerate after cross-section with preliminary application of a platinum mask with the use of a gas injecting system (GIS). The platinum mask is a heat sink and it also protects particle from melting and mechanical failure during ion beam etching. The image of particle after polishing (Fig. 1(c)) proves that the agglomerates have a porous cellular structure throughout.

Figure 2(a) demonstrates magnetic hysteresis loops of the examined powder. Note that the loops shape and the magnetization values practically coincide with the field dependences of magnetization of BFO nanopowders of size smaller than 40 nm reported in work [3]. The coercive force values at room temperature are also similar. The temperature dependence $H_C(T)$ exhibits a minimum near 100 K. An analogous $H_C(T)$ dependence is observed in nanocrystals [9] with a minimum at 50 – 60 K. The authors of work [8] attribute the $H_C(T)$ minimum to the transition of iron ions on the surface of nanoparticles to spin cluster glass state, which is confirmed by the exchange displacement of hysteresis loops. It is interesting to study the exchange displacement in porous spheres BFO. The inset in Fig. 2(a) shows $M(H)$ loops for ZFC and FC sample ($H_{FC} = 70$ kOe) at 2 K (the sample was field cooled from 300 to 2 K). It can be seen that the FC hysteresis loop is displaced towards negative field and positive magnetization, whereas in ZFC process the loop is centered around the origin of coordinates.

Note that the process of field cooling adopted in this study is not a traditional FC, since $T_N$ of BFO is much higher than 300 K. Thus, the exchange anisotropy established in this system without usual FC can be related to spontaneous effect of exchange displacement [7]. The dependence of $H_E(T)$ on cooling field of 70 kOe is presented in Fig. 2(b). As the temperature is raised, $H_E$ decreases abruptly and becomes equal to zero at $T > 100$ K.

If the minimum on the temperature dependence of $H_C(T)$ in the region of 100 K is related to the transition to spin glass state, then near this temperature there should be a temperature-dependent anomaly in the magnetization variation in ZFC mode.

Figure 3(a) demonstrates ZFC and FC magnetization curves of spherical agglomerates of BFO in 500 Oe field. As seen from Fig. 3(a), there is a divergence of ZFC and FC curves, which begins at 300 K and increases gradually with decreasing temperature. The observed splitting of the ZFC and FC curves at low temperatures is a distinctive feature
Spin-glass transition in porous spheres BiFeO$_3$

Fig. 1. a – Experimental (crosses), calculated (solid line), and difference (bottom line) XRPD patterns for BiFeO$_3$ and Si used as internal standard. Series of tick marks correspond to the Bragg reflections. b – SEM image of BFO agglomerates. c – SEM image of agglomerate after gallium ion beam polishing for 15 min. A platinum mask is applied on top of spin glass-like state and can be due to local spin clusterization [22]. In addition, we observe a sharp inflection on the ZFC curve at about 120 K, which can be ascribed to a typical blocking process of superparamagnetic spin moments assembly [23]. On the contrary, these moments are arranged parallel to the applied field during FC measurement, which leads to a large divergence of FC and ZFC curves below the freezing temperature. Similar changes in FC and ZFC are observed in BFO nanopowders [7–9]. A distinctive feature is that the maximum on the ZFC curve in nanoparticles is observed as a rule at a temperature of about 50 K.

The ZFC and FC magnetization characteristics of spherical BFO agglomerates were additionally studied by applying displacement magnetic field of different strength from 0.1 to 30 kOe. The splitting temperature $T_{irr}(H)$ (irreversibility in ZFC) in all fields was observed in the temperature range 250 – 300 K. We could not establish the field dependence of $T_{irr}(H)$ because of gradual divergence (perhaps this is due to the absence of heating above 300 K). The temperature dependences of ZFC magnetization in different fields are presented in Fig. 3(b).

The temperature ($T_m$) of ZFC plot, $M(T)$, is displaced towards lower temperatures when the magnetic field $H$ increases. For fields smaller than 10 – 20 kOe this displacement is described by Almeida–Thouless dependence (AT line):

$$H = A[1 - T_m(H)/T(0)]^3,$$

where $T_m(H)$ and $T(0)$ are the field dependence and the maximum temperature at $H = 0$, respectively. Eq. (1) establishes the boundary of transition to superparamagnetic state or the appearance of spin glass (AT line). As seen from Fig. 3(c), the $T_{max}(H)$ dependence can be divided into 2 parts: the first – in the interval 3 – 20 kOe; the second – in the interval 0 – 3 kOe. Data fitting by AT equation yields $T_1(0) = 97$ K for magnetic fields 3 – 20 kOe and
T_2(0) = 140 K for fields 0 – 3 kOe. An analogous inflection on the AT line in the region of 1 – 2 kOe is observed in films and nanocrystals [8, 24].

In order to find out, to which state the low-temperature phase corresponds, we measured the frequency-dependent variable of magnetic AC susceptibility [χ(ω, T)] in zero DC field.

Figure 4(a) shows the temperature dependences of the real part χ^1 of susceptibility to alternating field for porous spheres BFO at different frequencies at H = const ≈ 0. It is seen that the position of the χ^1(T) peak, corresponding to the freezing temperature T_f, is displaced towards higher temperatures with increasing frequency. The shift of the peak temperature χ^1(ω, T) was analyzed in terms of the empirical parameter of frequency-dependent sensitivity K = ΔT_f/(T_fΔln ω) (so-called Mydosh parameter), lying in the range 0.001 – 0.01 and 0.01 – 0.1 [25] for spin glass freezing and SPM blocking, respectively. In case of BFO, the K parameter turns out to be equal to 0.06, which is higher than in usual spin glass system and fits better SPM blocking. From Fig. 3(a) it is possible to obtain the temperature dependences of relaxation time τ = 1/2πf (Fig. 4(b)). Since the Mydosh parameter corresponds to SPM, then in accordance with the Neel superparamagnetic model the relaxation process should follow the Arrhenius equation [26]:

\[
τ = τ_0 \exp\left(\frac{E_a}{k_B T_f}\right),
\]

where τ_0 is the relaxation time constant, E_a is the anisotropy energy, and k_B is the Boltzmann constant. The results of fitting with E_a/k_B = 3249 ± 6 K and τ_0 = 2.3 · 10^{-15} are presented in Fig. 4(b). From the obtained values it follows that BFO spheres are not Neel SPM system [27], since for superparamagnetic relaxation τ_0 should be 10^{-10} – 10^{-13} s. The temperature dependence of relaxation time can be also approximated with the use of Vogel–Fulcher or
Spin-glass transition in porous spheres BiFeO$_3$

Figure 3. Almeida–Thouless line is shown by dotted line. a – Temperature dependences of FC and ZFC magnetization at values of magnetic field strength 0.5 KOe; b – Temperature dependences of ZFC magnetization at different values of magnetic field strength; c – Almeida–Thouless line (AT)

For the Vogel–Fulcher law [28]:

$$\tau = \tau_0 \exp\left[\frac{E_a}{k_B(T_f - T_{VF})}\right],$$

where $T_{VF}$ is the representative Vogel–Fulcher temperature. The best fit between $\tau(T)$ data and eq. (3) yields $E_a/k_B = 86 \pm 6$ K, $T_{VF} = 109 \pm 0.2$ K and $\tau_0 = (2.7 \pm 0.06) \times 10^{-5}$ s. For the power law [29]:

$$\tau = \tau_0 (T_f/T_g - 1)^{2\nu},$$

where $T_g$ is the glass transition temperature (static freezing temperature), $\nu$ is the critical index describing the correlation distance growth, and $z$ is the dynamic index describing the relaxation retardation. The power law is observed
at $T_g = 116 \pm 11 \text{ K}$, $\tau_0 = (6.7 \pm 0.13) \times 10^{-6} \text{ s}$ and $z\nu = 2.5 \pm 1$. The values of $\tau_{01}$ and $\tau_{02}$ for both power and VF laws fall in the typical category of cluster glass (CG) ($\tau = 10^{-5} - 10^{-10} \text{ s}$) for concentrated systems [30], rather than in canonical spin glasses in diluted systems. Thus, both the power law and V–F dynamics prove that the frequency-dependent anomaly in $\chi(\omega, T)$ of spherical samples BFO is related to the transition to cluster spin glass state.

![Graphs](image)

**Fig. 4.** a – The temperature dependence of the real part of AC magnetic susceptibility at different frequencies. The arrow shows the direction of frequency enhancement and the shift of the maximum. b – The temperature dependence of relaxation time

4. Conclusion

As a result of the research, it was established: (i) the presence of a minimum in the temperature dependence of $H_s(T)$ at 100 K and the appearance of an exchange bias increasing with decreasing temperature; (ii) FC and ZFC magnetizations differ greatly below 250 – 300 K; (iii) a maximum is observed in the temperature dependence of the magnetization ZFC at a certain value of $T_m$, and with an increase in intensity $H$, the value of $T_m$ decreases; (iv) a maximum near 120 K is observed on the temperature dependence of AC magnetic susceptibility, which shifts towards low temperatures when the frequency decreases. The intensity of the maximum of susceptibility lowers if frequency increases, which is typical of glass-like state that becomes less sensitive with enhancement of frequency.

The experimental data obtained in this work prove that in the temperature region of about 100 K there takes place a transition to spin glass state (or at least nonergodic behavior) in porous spheres BiFeO$_3$. The high values of relaxation time $\tau_0$ of the order of $10^{-6} - 10^{-5} \text{ s}$ allow one to draw a conclusion about the formation of cluster spin glass. The critical index describing the retardation of vitreous solid dynamics is $z\nu \approx 2.5$, which is much closer to the value obtained in the medium field system (where $z\nu \approx 2.0$) than in the classical Ising short-range model ($z\nu \approx 7 - 10$).

Note the presence of a knee on the $T_m(H)$ dependence in the region of fields 1 – 2 kOe. An analogous inflection is observed in nanopowders and films. The reasons of this inflection are not clear and require further studies.
As distinct from nanocrystals, porous spheres BiFeO$_3$ have a higher temperature of transition to spin glass state and at temperatures above the glass transition temperature there is no exchange displacement of hysteresis loops. There is also no phase transition to the ferromagnetic state at 5 K.

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