LIDAR-Assisted Wind Turbine Structural Load Reduction by Linear Single Model Predictive Control

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ABSTRACT Light Detection And Ranging (LIDAR) sensors provide preview measurements of wind speed in front of the device. This preview may be used to improve important aspects of the operation of wind turbines, such as structural load, while limiting the control effort. In this paper, a single model-based predictive controller, taking advantage of the incoming wind in advance LIDAR measurements, is applied to the generator torque reference of the wind turbine in order to reduce torsional shaft vibrations. The controlled system is tested in a simulation environment that reproduces a set of gusts and turbulent wind fields above the nominal, where the structural loads are higher. The performances obtained are compared with the baseline and with those extracted from a single model predictive controller version without disturbance previsualization. Then, the effect of the coherence between the effective wind estimated from the LIDAR measurements and the real wind is considered. The practical implementation is demonstrated on real-time controller prototypes applied to a Hardware-In-the-Loop Simulator that reproduces realistically the dynamic behavior of the National Renewable Energy Laboratory 5 MW reference wind turbine.

INDEX TERMS LIDAR, disturbance preview, feedforward control, model-based predictive control, hardware-in-the-loop simulation, load reduction, practical implementation, parameter uncertainty, real-time control, wind turbine.

I. INTRODUCTION

One of the main objectives of wind turbines (WT) control is to reduce fatigue and extreme loads on the drive train and blades, while keeping the control action limited and the generated power stable. Improvements in these aspects result in a longer lifetime for the turbine, as well as a reduction in maintenance, thus lowering the cost of energy. However, this is a difficult task, as the transients caused by the bursts and turbulence represent unknown disturbances to the controller. Feedback-based controllers can only compensate for such transients with a delay, when their effects are shown at the system outputs and the WT actuators propagate the corresponding generated control action. Such a delay could be compensated for by using a controller that includes feedforward action, but a sufficiently early preview measurement of such disturbances is required. A Doppler LIDAR may provide such a measurement.

The feedforward control to manage WT is first proposed in [1], using measurements from a weather tower, as LIDAR sensors were then still too expensive. Later, the use of optical fiber substantially reduced the costs, and LIDAR started to be used for remote measurements of incoming wind [2]. Since then, LIDAR-based turbine control has been studied for both below (region 2) and above (region 3) nominal winds. However, it was demonstrated -see [3] and [4]- that the improvements obtained in the energy capture did not compensate sufficiently the disadvantages associated with the LIDAR-assisted control (structural load and torque fluctuations) for WT in region 2. Therefore, much work has been focused on using LIDAR-assisted preview-based control to regulate the rotor speed and mitigate the structural loads in
region 3. In fact, the potential of this approach has been extensively demonstrated by using both the effective wind preview throughout the rotor for collective pitch control, [5]–[14], and on each blade for individual pitch control, [15]–[17]. In addition, the LIDAR-assisted control of the yaw or speed has also been studied to improve the extracted energy, [18], [19]. Comprehensive reviews of the related literature as well as critical discussions on the state of the art and future of the LIDAR-assisted wind turbine control may be found in [20]–[22].

The mentioned controllers range from simple feedforwards, based on inverse models -see e.g. [9]-, to more complex model predictive controllers (MPC). These MPCs use the previsualization of the disturbance caused by the incoming wind in order to optimize the control actions during the prediction horizon, avoiding to some extent the effects of the estimation delay, appeared in the controllers based on feedback [10], [14], [15], which causes a substantial improvement in the performance of the controlled system. However, it soon became clear that the improvement achieved in this way is largely conditioned by the quality of the effective wind measurement that can be taken in practice by the installed LIDAR. On the other hand, the LIDAR-assisted MPC faces the same practical implementation problems as the MPC without preview. The handling of highly non-linear wind turbine dynamics means that a trade-off between performance and computational load must always be made. Moreover, it is very difficult to ensure in advance the formal stability of such controllers and, even more, without drastically limiting their performance. A solution to these implementation problems is based on using a single linear model of the wind turbine in the internal prediction of the MPC, for the whole range of wind speeds in the region 3 -see reference [23] for further details-.

This work describes a Single Model Predictive Control (SMPC) controller that uses the same single linear turbine model and settings already presented in [23], but now also incorporating the prediction of the disturbance posed by fluctuations in the aerodynamic torque, caused by alterations in the incoming effective wind, realistically measured by a LIDAR system. The control goal again focuses on the reduction of the structural load on the transmission train, without excessively altering the generated power. The performance achieved by this controller is compared with the baseline and with one of those presented in [23]. Finally, such comparison is related to the quality of the available preview effective wind measurement.

The paper is organized as follows: Section II presents how the incoming disturbance is extracted from the measurements obtained in advance by the LIDAR and explains how it fits into the SMPC approach, described in [23] for the case when no disturbance previsualization is available. Then, Section III summarizes the comparative results obtained from a perfect disturbance previsualization in order to study the potential performance of the proposal. To do so, the National Renewable Energy Laboratory (NREL) 5 MW reference turbine is exposed to coherent gusts and three-dimensional stochastic wind fields. Such a study is carried out based on both numerical simulations and using real-time controller prototypes, applied to the Hardware-in-the-Loop (HiL) wind turbine simulator, also used in [23] but conveniently modified. In section IV, the obtaining of realistic LIDAR measurements is described, and, in Section V, the reduction on the structural load, obtained as a function of the quality of the LIDAR preview, is presented and commented. Finally, Section VI concludes the paper with a summary and the future perspectives of the work.

II. LIDAR-ASSISTED LINEAR SMPC

The SMPC controllers presented in [23] use a single internal linear model to obtain the behavior of the WT rotor and drive-train during the prediction horizon. Such a model is a three-mass model, for the mechanical part, in series with the dynamic model of the generator electric behavior. The mechanical model considers the inertia of the effective flexible part of the blades \(J_{bl}\), the inertia of the rigid part of the blades plus the hub \(J_{hub}\) and the inertia of the generator \(J_{gen}\). Such three masses are linked by two flexible elements representing the stiffness and damping of the blades and drive-train. The inputs to the internal model are, at one end, the aerodynamic torque \(T_{aero}\) that the incident wind applies on the blades and, at the other, the generator torque reference \(T_{em}^{*}\), provided by the controller. \(T_{aero}\) is considered a measured disturbance (MD) and \(T_{em}^{*}\) is the manipulated variable (MV). When no measurements of the effective wind \(W_m\) on the rotor are available, the aerodynamic torque \(T_{aero}\) must be estimated from its effects on the angular speed of the generator \(\omega_{gen}\). This may be done either by external preprocessing or by taking advantage of the MPC state observer -see section III. D. in [23] for details-. In both cases, the estimation suffers from a certain delay that impairs the performance achieved in reducing the structural load.

Now, we assume that the incoming wind measurements obtained through a LIDAR focused at a certain distance from the rotor are used to calculate the effective wind \(W_m\) that will affect the WT, with some anticipation. This anticipation depends namely on the focal distance and the average speed of the wind, and the assumption is made that it will be greater than the duration of our SMPC prediction horizon. Obviously, it will be also necessary to estimate the aerodynamic torque \(T_{aero}\) that such effective wind \(W_m\) will induce in our rotor of radius \(R\). In order to do so, the reduced aerodynamic model, already presented in [23], is utilized:

\[
T_{aero} = \frac{1}{2} \rho \pi R^3 C_P(\lambda, \beta) W_m^2 = 0.5 \rho \pi R^2 W_m^3 \frac{C_P(\lambda, \beta)}{\omega_{rot}}
\]

where \(\lambda\) is the speed ratio, \(\omega_{rot}\) the angular speed of the rotor and \(C_p\) the effective power coefficient, implemented as a look-up table and extracted from steady-state simulations of the NREL 5MW turbine with WT_Perf [24].
The processing of the model (1) that allows implementing the $T_{\text{aero}}$ preview starts with the accumulation in buffers of enough input data to fulfill its evolution during the prediction horizon ($N$ samples). It is clear that we do not have future values for the pitch angle $\beta$ and rotor speed $\omega_{\text{rot}}$, since they depend on the action of the pitch control loop that is not included in the model. However, the dynamic behavior of that loop and, therefore, of those variables, is much slower than the control of the torque of the generator we are dealing with. This allows us to update, at each sampling time, the complete content of such buffers with the $N$-times repeated current measurement of such variables.

As can be seen in Figure 1, the model (1) is computed to obtain, at each sampling instant, the preview of $T_{\text{aero}}$, defined as a measured disturbance (MD) in the SMPC. Later, this preview is introduced in the internal model, giving rise to an approach similar to the version 1 of the SMPC controller described in section III. D. 1. of [23]. In that case, as no disturbance preview was available, the disturbance was considered equal to the last calculated value over the whole prediction horizon. Since this calculation is always obtained with a certain delay, the control action cannot anticipate the arrival of important changes in the incident wind. However, by having a preview of the disturbance, the controller may predict the effect on the system in time to compensate for the control action delays (algorithm execution, instrumentation, actuator,...), improving in many cases the resulted performance, without the need to increase the control action.

As in that case, the internal model is also provided with an additional input $\Delta T_{\text{aero}}$–see figure 1-, defined as an unmeasured disturbance (UD1), in order to give robustness to the approach, given the errors prone to occur in the $T_{\text{aero}}$ previewer. These errors can take place due to multiple causes, namely, the aerodynamic model of the turbine, the measurement of the effective wind $W_{\text{m}}$ and the approximation made for the “prediction” values for $\beta$ and $\omega_{\text{rot}}$. Assuming that such errors may turn out to be persistent, the SMPC internal model is extended with a new state –an integrator is used as an input disturbance model for $\Delta T_{\text{aero}}$ and the Kalman filter, incorporated in the SMPC controller, is in charge of estimating its value. The same procedure may be used to estimate the entire input unmeasured disturbance, not only the errors made in its calculation, and obtain good control results. In fact, the alternative controller version SMPC UD, which is used for comparison in this study, works in this way –see section III.D.2. of [23] for details-.

**Note 1:** Observe that the preview calculation described above requires the use of a nonlinear function to calculate the $C_p$ effective power coefficient. However, this calculation is implemented outside the internal model of the MPC controller, thus allowing us to maintain the use of a single linear internal model and the advantages that this entails. Note that these advantages include a low computational burden and, most importantly, the in advance proof of stability based on the application of a terminal weight on the system states. Such terminal weight is obtained easily from a simple matrix Lyapunov equation and does not represent a notable limitation on the performance of the controlled system –see section III. C. of [23] for details-.

### III. CONTROLLER POTENTIAL PERFORMANCE

In this section, it will be assumed that the effective wind calculated from the LIDAR measurements coincides exactly with the real one. This is carried out to make the effect of disturbance previsualization more apparent and better analyze the reachable potential (maximum) performance. First, the comparative results are obtained using numerical simulations. Then, the modifications made in the HiL simulator of the NREL 5 MW WT, used in [23], are described. Such modifications allow the real-time implementation of the LIDAR-assisted version. Finally, we present the comparative results obtained in such experimental testing. In both studies, the settings that impose the aggressiveness of the controller and the speed of the state observer are the same as those used in [23].

### A. SIMULATION RESULTS

For this controller with disturbance preview, the most important improvements may be expected in the reduction of extreme loads when wind gusts episodes occur. However, it can also significantly reduce fatigue loads and, therefore, both cases are investigated in this section.

#### 1) EXTREME LOADS

As in section IV. A. in [23], hub height time series have been created with extreme operation gusts according to IEC standard [25] at $v_{\text{rated}} + 2 \text{ m/s} = 13.2 \text{ m/s}$ and $v_{\text{out}} = 25 \text{ m/s}$, being $v_{\text{rated}}$ and $v_{\text{out}}$ the rated and cut-out wind speeds for the NREL 5MW WT, respectively. Then, the performance of the LIDAR-assisted (MDL) and the compact version 2 (UD) –see section III. D. 2. in [23]- SMPC controllers are compared with the baseline in Table 1. Besides, in order to check the robustness to modeling errors, increments on the mass (ice, dust, ...) of the rotor has been considered. Specifically, changes on $J_{\text{bl}}$ and $J_{\text{hub}}$ inducing a 10 % alteration on the natural frequencies of the mechanical system have been
introduced in the WT model and the related results added to such comparison.

Specifically, the maximum (MaxTLSS) and standard (σ) deviations (% reduction with respect to baseline) on the torsional torque on the low-speed turbine shaft (TLSS) are presented in Table 1. The improvement obtained by MDL control is very high with respect to the baseline case, but not much greater than that achieved by the UD controller, without preview. This is probably due to the intense adjustment of the state observer used here. Such adjustment manages to reduce to the minimum the delay in the internal estimation of the \( T_{aero} \) disturbance. Furthermore, as expected, it is also noted in Table 1 that the robustness to modeling errors is better in the UD controller, given that its performance does not depend so much on the internal model by having more feedback action.

### TABLE 1. Percentage reduction in TLSS for extreme loads.

| Results | Numerical Simulations | Real-Time Experiments |
|---------|----------------------|-----------------------|
| Model error | 0 %   | 10 %   | 0 %   | 10 %   |
| GDP version | MDL | UD | MDL | UD | MDL | UD |
| \( \sigma \) (MaxTLSS) | -48.1 | -48.4 | -26.6 | -96.3 | -97.3 | -41.7 | -54.6 | -52.3 |
| \( \sigma \) (\( \sigma_{\text{LSS}} \)) | -89.0 | -89.7 | -43.9 | 97.6 | -90.0 | -49.3 | -82.9 | -60.4 |

2) **FATIGUE LOADS**

As in section IV.B in [23], to evaluate the fatigue load, a set of A-type turbulent wind fields according to IEC 61400-1 [25] in full-load operation region (mean wind speeds of 14, 18 and 24) generated with TurboSim [26] has been applied to the simulation environment. Then, the lifetime Damage Equivalent Loads (DEL) for the low-speed shaft torsion torque (TLSS) were calculated on the basis of a rainfall counting with Wohler exponent of 4, typical for steel generator shafts [27]. The maximum (DEL), standard (σ) TLSS deviations (% reduction to baseline), and power mean increase were also computed and presented in Table 2. The observed fatigue load reduction in slightly better in the LIDAR-assisted case, and the robustness is conserved.

### TABLE 2. Percentage reduction in TLSS for fatigue loads.

| Results | Numerical Simulations | Real-Time Experiments |
|---------|----------------------|-----------------------|
| Model error | 0 %   | 10 %   | 0 %   | 10 %   |
| Wind 14 m/s | MDL | UD | MDL | UD | MDL | UD |
| \( \sigma \) (DEL) | -89.3 | -93.2 | -82.5 | -90.9 | -88.7 | -56.2 | -81.1 | -57.7 |
| Mean POW | 0.87 | 0.78 | 0.81 | 0.87 | 0.72 | 0.66 | 0.66 | 0.72 |
| Wind 18 m/s | MDL | UD | MDL | UD | MDL | UD |
| \( \sigma \) (\( \sigma_{\text{LSS}} \)) | -94.5 | -92.7 | -85.6 | -93.1 | -85.9 | -46.9 | -80.3 | -52.2 |
| Mean POW | 0.07 | 0.08 | 0.14 | 0.14 | -0.03 | 0.05 | -0.03 | 0.07 |
| Wind 24 m/s | MDL | UD | MDL | UD | MDL | UD |
| \( \sigma \) (DEL) | -90.6 | -88.4 | -72.1 | -83.7 | -81.8 | -33.7 | -70.6 | -27.0 |
| Mean POW | 0.16 | 0.17 | 0.15 | 0.17 | 0.00 | 0.13 | 0.02 | 0.14 |

**B. ADAPTED REAL-TIME EXPERIMENTAL PLATFORM**

The Real-Time (RT) control experiments are implemented on the hardware platform described in [23], section V. It is composed conceptually by two elements: a WT Hardware-in-the-Loop (HIL) simulator, that reproduces the scaled behavior of the 5 MW NREL turbine on a mechanically coupled motor-generator set, and a rapid-prototyping system, devoted to put the turbine controllers into action and analyze their computational burden. The WT HIL simulator uses RT software to compute the aerodynamic and mechanical turbine models and, then, an electric motor to impose the resulting action on the generator shaft. On the other hand, the RT control platform implements the pitch, the generator, and the grid-side converter controllers. Anyway, given that the LIDAR-assisted version of the SMPC controller needs some new inputs (β and the wind preview \( W_a \) from the LIDAR), the experimental setup is correspondingly modified.

The block diagram explaining the modified platform is presented in Figure 2, where the LIDAR block is dedicated to prepare the SMPC controller effective wind previsualization \( W_a \). By now, such a preview is identical to the delayed signal \( W_a \), created with TurboSim, feeding the aerodynamic model located inside the HIL WT simulator. Evidently, such delay matches the prediction horizon used in the SMPC controller.

**FIGURE 2.** Adapted experimental platform scheme.

**C. REAL-TIME CONTROL EXPERIMENTS RESULTS**

The same experiments described in section III.A have been implemented in deterministic real-time (RT) on the described experimental platform. Anyway, both control and observer setup have been relaxed – exactly as in [23] – in order to reduce the disturbances on the generated power and attain a more robust behavior for the controlled system under intense measurement noise.

1) **EXTREME LOADS**

The signals of interest, measured in the RT experimental platform, when applying the two SMPCs and the baseline controller under an extreme operation gust, according to IEC standard, at \( v_{out} = 25 \) m/s, are depicted in Fig. 3. Namely, the actual pitch angle \( \beta \), the rotor angular speed \( \omega_{rot} \), the generator torque \( T_{em} \), the torsional torque referred to the low-speed shaft TLSS and the mechanical power \( (T_{em} \omega_{gen}) \) are presented.
Note 2: Note that the actual pitch $\beta$ has been extracted from the RT execution of the pitch actuator model in the WT HiL simulator and then provided as a voltage input to the RT control prototype, in order to emulate a blade angular position sensor output. The $\omega_{rot}$ is derived from the measured $\omega_{gen}$, $T_{em}$ is obtained from the measured currents on the generator machine ($i_{sq}$) and the mechanical power by multiplying such measured $\omega_{gen}$ and $T_{em}$. In this way, the RT control results incorporate the effects of the common WT instrumentation. Anyway, nowadays the wind turbines often incorporate additional sensors, e.g. in the hub for $\omega_{rot}$, or strain gauges in the root of the blades, from which the $T_{blades}$ torque of our internal model can be obtained -see Figure 1 and [23] for details-. Such signals may be also emulated by hardware in the context of our WT HiL simulator, as it is done for $\beta$, to provide more measured outputs to the SMPC controllers. In this way, the robustness against modeling errors could be substantially improved and the important effect of the realistic measurements better taken into account.

To facilitate a clear analysis of the disturbance previsualization effect in Fig. 3 and 4, errors in the internal model are avoided in these RT experiments and a detailed comparison of the manipulated variable $T^*_{em}$ is presented in Fig. 4. It is evident that the control action of the MDL version -see temporal evolution of the manipulated variable $T^*_{em}$- anticipates the appearance of the disturbance -wind gust-, reducing the torsion of the axis with respect to the UD case, in which this preview is not available. Moreover, such an important improvement is obtained without increasing notably the variation of the generated mechanical power with respect to the UD case.

Next, to study the robustness to model parameter uncertainty, as in section III. A, an increment in the rotor inertia, producing a 10% error in the torsional frequencies of the internal model of the SMPCs, is introduced. Again, the same signals of interest, obtained by the two SMPC versions and the baseline controller under extreme down ($v_{rated}+2$ m/s = 13.2 m/s) operation gust, according to IEC standard, are depicted in Fig. 5. Besides, Table 1 presents the experimental load reduction (in %) with respect to the baseline, numerically.
The obtained reduction on the extreme loads on the torsional torque on the low-speed shaft \(T_{LSS}\) -and the corresponding vibrations on the transmission train-, thanks to the LIDAR disturbance previsualization, are again apparent on Fig. 5 and, numerically, in Table 1, even with an important error in the model. Thus, the SMPC-MDL robustness to model parameter uncertainty is demonstrated.

On the other hand, Table 1 shows that the significant drop in performance suffered by the UD version of the SMPC when relaxing the settings of the controller and state estimator with respect to the simulation-based study -see [23] for more details-, does not take place in the LIDAR-assisted version (MDL). It is probably due to the effect of the anticipation of the control action that allows maintaining the performance despite using a less aggressive setting.

2) FATIGUE LOADS
The responses to the 15 % turbulent wind of mean speed of 24 m/s, when a 10 % error is present in the internal model of the SMPC versions, are now displayed in Fig. 6. In addition, Table 2 presents the obtained improvements in a comparative numerical way. The experimental platform needs 30 seconds to reach Region 3 and, at the second 39, the SMPC controllers are activated to reduce the load.

**FIGURE 6.** Experimental performance on turbulent wind at 24 m/s with 15 % of turbulence and 10 % internal model error: Baseline control (black), SMPC versions MDL (blue) and UD (red).

Again, the obtained improvement by the SMPC-MDL version, based on the perfect previsualization of the incoming effective wind on the rotor, is very high, doubling the drive-train load reduction gained by the UD version. The robustness to model errors seems to be also very high.

IV. REALISTIC LIDAR MEASUREMENTS

A. BACKGROUND
Early work on LIDAR-assisted control [5], [7], [28] assumed that incoming winds could be measured exactly. Thus, it is supposed to be no difference between the measured and actual effective winds and there is no error in the calculation of the instant that such wind reached the rotor. Later, realistic LIDAR models started to be used [7], [29]. Such models included the spatial averaging of the measurements and the limitation of the line-of-sight. In addition, the wind evolution is also included as a source of error in other works [13], [14], [16], taking into account how the wind changes from the time it is measured until it impacts the rotor. Some papers [12], [30] also consider the uncertainty in the calculation of the instant in which the wind actually reaches the rotor.

It is clear that implementing a feedforward-based control, when the preview signal includes too much error, implies some risk, since the controller reacts to such error, turning its action into something potentially counterproductive. Therefore, many recent works, focused on the design of LIDAR-assisted controllers [9], [31], propose characterizing the measurement error and filtering the signal to eliminate the components that do not maintain sufficient correlation with the effective wind, actually reaching the rotor. Besides, others [11], [33] propose to include such correlation directly in an optimal control scheme.

On the other hand, it has been shown [32], [34] that, by soundly manipulating the preview obtained from the LIDAR measurements, it is possible to notably improve the estimate that can be made of the disturbance that the incoming wind will actually cause in the rotor. Specifically, in Simley et al. [32] –see also [21] and [36]–, a minimum mean square error (MMSE) estimate of the effective approaching wind can be obtained by using an optimal filter whose design depends on the mentioned correlation between the LIDAR measurement and the actual disturbance. To calculate such correlation, the true wind disturbance must be estimated [35], by roughly using the turbine as an anemometer. In these works, the mentioned filtering should cover the control actuator bandwidth, that is, up to 1 Hz. Very recently, an artificial neural network (ANN) trained online is used in [37] to soundly correct the errors of the LIDAR previsualization.

B. REALISTIC LIDAR MEASUREMENTS GENERATION
For wind speeds above nominal, the WT control goals are focused on regulating the rotor speed and minimizing the structural load, while keeping the control action limited. Achieving such goals allows the turbine lifetime to be notably increased and, therefore, the cost of energy to be reduced. The benefit of using a LIDAR sensor in order to achieve such control objectives depends on the measurement coherence, that is, the correlation as a function of frequency between the anticipated wind measurement and the one that the turbine will actually receive.
Our aim now is to use a method, well established in the literature, to generate realistic LIDAR measurements with different quality levels. Then, such measurements are used in the real-time control experiments in order to determine the impact of the LIDAR measurement quality on the SMPC control performance. The main finding will be to determine how good these previews must be for the performance to be good enough in order to justify the use of a LIDAR sensor.

One way to define formally such measurement coherence as a function of frequency \( f \) is given by

\[
\gamma_{am}^2(f) = \frac{|S_{am}(f)|^2}{S_{aa}(f)S_{mm}(f)}
\]

where \( \gamma_{am}^2(f) \) is the magnitude squared coherence, \( S_{am}(f) \) is the cross power spectral density between the measured \( W_m \) and the actual \( W_a \) experienced by the turbine. Such wind \( W_a \) is estimated by an observer using the turbine itself as an anemometer [35]. Normally, such a method provides a good estimate up to frequencies covering the bandwidth of interest. On the other hand, \( S_{mm}(f) \) and \( S_{aa}(f) \) are the individual power spectral densities of the measured and actual signal, respectively.

Such squared coherence magnitude can go from one to zero, where one indicates perfect correlation. Therefore, a correlation of less than one means that the measurement includes errors that, in this case, maybe due to measurement noise, wind evolution occurred from focal length, and WT induction zone. The mentioned last two errors are more important at high frequencies, causing the coherence to go normally from values close to one at low frequencies to values close to zero at high frequencies. The exact shape of the coherence function depends on the configuration of the LIDAR sensor and wind and environmental conditions. Evidently, such function shape may be also altered if some advanced method, like those described in [32], [37], is applied to the sensor output to improve the coherence of the signal.

In order to study the influence that the quality of the \( T_{aero} \) preview, extracted from in advance incoming wind measurements, has on the performance of the LIDAR-assisted SMPC, the method, proposed in Dunne and Pao [33], to generate realistic LIDAR measurements with different coherence profiles, will be here followed. In such motivating work, the actual wind \( W_a \) is generated and, after the preview delay, applied to the WT aerodynamic model. Meanwhile, the wind measured by the LIDAR \( W_m \), which is then sent to become an input to our SMPC MDL controller –see Figures 1 and 2–, is calculated according to

\[
W_m = LW_a + Hn
\]

where \( L \) is a low-pass filter, \( H \) is a high-pass filter and \( n \) is white noise. Filters \( L \) and \( H \) are designed to achieve that the coherence shape, as a function of the frequency, between \( W_m \) and \( W_a \), is the desired one and that the power spectrums of both signals match, that is, \( S_{aa} = S_{mm} \). It is convenient that \( S_{aa} = S_{mm} \) because the difference in power spectrums could affect the controller gain. So, we have –see [33]–

\[
|L| = \sqrt{\text{coh}(f)} \quad (4)
\]

\[
\angle L = 0 \quad (5)
\]

\[
|H| = \sqrt{|W_a|^2 (1 - |L|^2)} \quad \angle H = \text{irrelevant} \quad (6)
\]

where \( \text{coh}(f) \) is the coherence of the LIDAR-based measurement, defined as in the expression (2), that we wish to obtain between \( W_m \) and \( W_a \). The magnitudes for the \( H \) and \( L \) filters obtained by expressions (4) and (6) ensure that the coherence shape is \( \text{coh}(f) \) and that \( S_{aa} = S_{mm} \). The phase for filter \( L \) in expression (5) ensures that the average phase between \( W_m \) and \( W_a \) is zero, which is the case when we have correctly calculated and imposed the preview time.

As in [33], a Butterworth low-pass filter of order 1 is used for \( L \). Then, several coherence target functions, for different bandwidths (cutoff frequencies, where the magnitude of the filter response is \((0.5)^{1/2}\) of its DC value) of interest for our filter \( L \) are obtained. Using such coherence functions, digital filter \( L \) is calculated by applying expression (4). However, it is impossible to obtain a causal filter that also meets the condition (5). To roughly solve this problem, the phase of \( L \) is approximately converted first to a time delay, extracted by using a very low frequency of the bandwidth. Then, such delay is added to the preview delay applied to \( W_a \) before it feeds the aerodynamic model –see figure 2-.

\[
C. APPROACH AND BANDWIDTH RANGE
\]

This study on the impact of the LIDAR coherence does not apply to extreme loads, since the prediction of gusts is hardly affected by the considered measurement errors, given the spectral content of such gusts. Therefore, only the reduction of fatigue load caused by turbulent wind in the transmission train is considered here. More precisely, the aim of our approach relies on how the performance of the LIDAR-assisted SMPC control is affected by the preview errors, within a plausible range, for turbulent winds in region 3.

Since the present approach needs a scenario as realistic as possible, the control experiments have been exclusively performed on the NREL 5MW WT HiL Simulator. Such WT HiL simulator has been described in section III. B and used to obtain the experimental results presented in section III. C., for the ideal LIDAR case. Besides, the SMPC controller and state observer settings are the same as those used in section III.C and the version MD without preview [23]. However, the design of the LIDAR block in the WT HiL simulator –see Figure 2-, that was transparent \((W_m = W_a)\) then, has now been altered. For the present study, such block implements the operation described in section IV. B and defined by expressions (3)-(6), according to the scheme shown in Fig. 7.

On the other hand, using the LIDAR patterns studied by Schlipf [38] for the NREL 5MW WT, the coherence bandwidth (BW) range can reach 0.2186 Hz. In the best case, for
the LIDAR configuration used there -see also [33]-. However, given the mentioned works of Simley et al. [32], [35], [36], in this study the bandwidth of interest has been extended up to 1 Hz, that is, the bandwidth of the pitch actuator, as it is where their method based on optimal filters may provide sufficient coherence. In our case, the preliminary idea is that the generator torque SMPC control system under study here could take advantage of a preexistent LIDAR preview taken for a pitch feedforward control system -for example, those described in [9], [33], [36] that may be working in parallel. Of course, the settings of a LIDAR sensor may be reconfigured in order to optimize the in advance wind measurements for its use with the load reduction SMPC controller. Besides, it is probable that, in such a case, a broader bandwidth for the wind previsualization could be obtained.

V. REALISTIC PERFORMANCE FOR THE LIDAR-ASSISTED SMPC (REAL-TIME CONTROL EXPERIMENTS RESULTS)

A. EXTREME LOADS

As stated before –see section IV. C-, the experimental real-time control results remain approximately the same for realistic previews of the incoming wind –see section III.C.1-.

B. FATIGUE LOADS

The HiL Simulator for the NREL 5 MW WT has been fed with turbulent winds, generated again with Turbsim [26], of 14, 18 and 24 m/s, of average speed and turbulences of 18 %, 17 % and 15 %, respectively. The corresponding realistic LIDAR readings have been generated following the procedure described in section IV. The obtained results for the torsional load of the turbine shaft have been processed to calculate the DELs that describe the fatigue load. Then, the experimental tests have been repeated considering an internal model with an error in the natural vibration frequencies up to 10 %. The results regarding the DEL percentage improvement, with respect to the baseline control, of the LIDAR-assisted SMPC controllers, are presented in Figures 8, 9 and 10, for the three mentioned average wind speeds, respectively. The bandwidth -cutoff frequencies, where the magnitude of the L filter response is \((0.5)^{1/2}\) of its DC value- of the LIDAR previsualization used by the SMPC-MDL is in the Y-axis. Within such bandwidth, the magnitude squared coherence, between the anticipated wind measurement and the one that the turbine is actually experiencing, is supposed to be sufficiently good. The improvements obtained by using an ideal LIDAR (BW INF Hz) and SMPC-UD (say, BW 0Hz) is also incorporated to that axis as limiting references.

Note 3: When the LIDAR previsualization gives no useful information about the stochastic nature of the incoming wind (BW = 0 Hz.), the wind preview \(W_m\) may be described as a DC offset (wind average speed) plus white noise. In such a case, given the structure of the SMCP LIDAR-assisted version –see Fig. 1-, the additional input \(\Delta T_{aero}\) defined as an unmeasured disturbance (UD1), represents now the whole \(T_{aero}\) and the SMPC Kalman Filter remains in charge of estimating it. In this way, the SMPC MDL version “converges” to the UD version, when the LIDAR measurements coherence is completely lost.
Therefore, it may be seen in Figures 8-10 how the quality of the wind preview affects the comparative performance of the LIDAR-assisted SMPC-MDL version, related to the performance achieved by the UD version -without preview-. By considering preview coherence bandwidths between 1 and 0.0125 Hz, it is clear that the obtained load reduction monotonically decreases, as the preview coherence decreases, from the ideal LIDAR (perfect preview) to the SMPC-UD (no preview) case. The robustness to model parameter uncertainty behaves in a very similar fashion.

Anyway, it turns out to be crucial to obtain sufficiently reliable LIDAR measurements of the incoming wind to justify the use of the preview-assisted SMPC option. In particular, for this case study, it seems mandatory to apply some technique in order to improve the quality of the preview for high frequencies (up to 0.75 Hz.-1 Hz.), as those described in [21], [32], [36] and, very recently, [37]. Only by obtaining sufficient coherence in such bandwidths, the obtained reductions in the drive train load are big enough to justify the use of LIDAR.

Finally, the responses to the 15 % turbulent wind of mean speed of 24 m/s, when a 10 % error in the internal model of the SMPC versions is present, and a LIDAR preview with 1 Hz. coherence bandwidth is used, are now displayed in Fig. 11. Again, the experimental platform needs 30 seconds to reach Region 3, and, at second 39, the SMPC controllers are activated to reduce the load. Right then, it may be seen how, indeed, the torque on the shaft $T_{LSS}$ is remarkably stabilized with respect to the baseline case and the SMPC UD version. The vibrations associated with natural frequencies related to the flexibility of the main mechanical components of the turbine are also largely eliminated from the pitch angle $\beta$ and rotor speed $\omega_{rot}$. On the other hand, the generator torque $T_{em}$ activity is significantly increased compared to the baseline control and this, in turn, is partly transferred to the generated mechanical power $T_{gen}$. However, as we may observe, by comparing Fig. 6 and 11 –and also in Fig. 10–, the load reduction when a LIDAR preview coherence bandwidth of 1 Hz., is only slightly impaired with respect to the perfect preview case (70.59 to 67.17 % load reduction). Even more, the control effort in $T_{em}$ and the corresponding disturbance in the generated mechanical power has been reduced.

To verify this effect, Figure 12 shows the electric power measured by the REGEN Unidrive unit in the NREL WT 5MW HiL Simulator hardware –scaled-. As we can see, the power provided to the grid, when a realistic LIDAR preview is used, seems less disturbed than when using a “perfect” preview or even the SMPC UD version, without wind previsualization. Therefore, if an effective wind preview, with sufficient coherence up to about 1 Hz, is achieved, the use of LIDAR-assisted SMPC control is fully justified.

At this point, in order to further confirm such important assertion, it seems appropriate to complete the study with a frequency analysis of the signals of interest presented in Figures 11 and 12. Therefore, the Fast Fourier Transforms (FFT) of such signals have been calculated and presented in Figure 13. In such a figure, it may be seen that the effects of the torsional vibrations on pitch angle, generator speed, and low-speed shaft torque are greatly attenuated. It may also be seen that the power of some frequency components is increased to some extent in the generator torque and, correspondingly, in the generated mechanical power. However, we may also see that the frequency components of the generated electrical power, supplied to the grid by the three controllers on the comparison, are very similar.

Note 4: Let’s look one more time, in figure 13, at the generated power FFTs, both mechanical and electrical. It may be seen that only the very low-frequency components (below 0.75 Hz., approximately) of the increase in the disturbances, observed in the mechanical power -due to the control action-, pass clearly through the DC bus to reach the electrical power, supplied to the grid. This effect can also be seen in
Such disturbances, as shown in figure 11, are caused by the low-frequency oscillations in \( \omega_{rot} \), due to the performance of the pitch control loop, which are then transferred to \( \omega_{gen} \), and, finally, to the generated power. Fortunately, these observed fluctuations in the electrical power are relatively small in magnitude —see figure 12—. However, if necessary, they could be avoided when applying the SMPC controllers, by renouncing -partially or totally- to prevent their impact on the torsion of the shaft. In order to do this, we should inject such low-frequency fluctuation -in counter phase- into the SMPC low-speed shaft torque reference \( T^\ast_{LSS} \) via \( \omega_{genf} \) (remember, \( T^\ast_{LSS} = P_{rated}/\omega_{rot} = P_{rated}N_{gear}/\omega_{genf} \)). By now, \( \omega_{genf} \) is fixed at the \( \omega_{gen} \) nominal value, given that the present study aims to analyze the SMPC capacity to reduce at a minimum the WT structural load. Now, alternatively, to obtain \( \omega_{genf} \), we may low-pass filter \( \omega_{gen} \) measurement by using cut-off frequencies around 1 Hz. -see FFTs of the generator powers in figure 13- and add the result in counterphase to the \( \omega_{gen} \) nominal value. In this way, it would be possible to importantly reduce the fatigue load on the transmission train originated by the elasticity of the shaft and rotor (1.7 and 4 Hz.), while allowing —partially or totally, at will— the low-frequency shaft torsion in order not to convert such mechanical vibrations into electrical ones. By designing the low-pass filter -cutoff frequency and order- used to produce \( \omega_{genf} \), we may balance the partial transmission of such mechanical vibrations into electrical ones. By design- and rotor (1.7 and 4 Hz.), while allowing –partially or totally, the transmission train originated by the elasticity of the shaft —see FFTs of the generator powers in figure 13— and add the \( \omega_{genf} \) capacity to reduce at a minimum \( P_{rated} \).

C. COMPUTATIONAL BURDEN

The real-time controllers have been implemented on an Intel Core2 Duo E8400 3 GHz industrial computer equipped with Simulink Real-Time —see [39]- kernel. The KWIK algorithm —see [40]- has been used to solve the optimization quadratic problem. The SMPC controllers have been implemented by using a standard 80 Hz. sampling frequency. The maximum computational delays for de LIDAR-assisted version was 5,129e-5 s., corresponding to a maximum number for iterations of 7. On the other hand, the more compact UD version has given a maximum computational delay of 3,41e-5 s. with 4 iterations at most. In both cases, the computational burden does not reach 0.4 % and, therefore, the corresponding delay is negligible. Further details are available in [23].
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