Supporting information on “Verwey-type charge ordering and site-selective Mott transition in Fe$_4$O$_5$ under pressure”

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Experimental Methods

Samples of Fe₄O₅ were synthesized using a 1200-tonne Multi-Anvil Press at BGI [1] at HP-HT conditions from stoichiometric mixtures of fine powders of Fe₃O₄ and iron (both from Aldrich company, 99.999% purity). These syntheses were performed at pressures of about 14 GPa over several hours. High-quality single crystals with linear sizes of about 20–250 μm were synthesized at high temperatures in the range of 1350–1450 °C [2]. We employed a standard multi-anvil assembly that included a Re cylindrical sample capsule, a LaCrO₃ heater, W3Re/W25Re thermocouple, and other components packed inside an octahedron made of 5% Cr₂O₃-doped MgO [3]. The synthesis procedure was similar to the one described in previous works [2, 4]. The chemical composition of the samples was verified in a microprobe analysis using a JEOL JXA-8200 electron microscope. The crystal structure of the samples was determined using single crystal and powder X-ray diffraction (XRD) on a high brilliance Rigaku diffractometer (Mo Kα radiation, λ = 0.7108 Å).

X-ray diffraction studies

Data collection

Run 1. The data collection was carried out at the ID15B beamline at the European Synchrotron Radiation Facility (ESRF), Grenoble, France (MAR555 flat panel detector, λ = 0.41114 Å, beam size 10(V) × 10(H) μm²). Sample-to-detector distance, coordinates of the beam center, tilt angle and tilt plane rotation angle of the detector images were calibrated using Si powder. XRD wide images were collected during continuous rotation of DACs typically from –20° to +20° on ω; while XRD single-crystal data collection experiments were performed by narrow 0.5° scanning of the ±32° ω range. A black single crystal of Fe₄O₅ with dimensions of 0.02 × 0.02 × 0.01 mm³ together with a small ruby chip (for pressure estimation) were loaded into LeToullec membrane-driven type DAC [5] equipped with Bohler-Almax diamonds with 300 μm culet size. A hole with diameter about 150 μm in steel gasket pre-indentent to 40 μm was served as a pressure chamber. Neon was used both as a pressure transmitting medium and as a pressure standard [6].

The DAC was compressed to 46.8(5) GPa with wide and step scan images being collected at each pressure point. Processing of XRD data (the unit cell determination, integration of
the reflection intensities, empirical absorption correction) were performed using CrysAlisPro software [7]. A single crystal of an orthoenstatite \([\text{Mg}_{1.93}\text{Fe}_{0.06})\text{Si}_{1.93}\text{Al}_{0.06})\text{O}_6\], space group \(Pbca\) with \(a = 18.2391(3), b = 8.8117(2),\) and \(c = 5.18320(10) \text{ Å}\), was used to calibrate the instrument model of CrysAlisPro (sample-to-detector distance, the detector’s origin, offsets of the goniometer angles and rotation of the X-ray beam and the detector around the instrument axis).

**Run 2.** In the second attempt we loaded a mixture of \(\text{Fe}_3\text{O}_4\) (with purity 99.997\% purchased from Alfa Aesar (LOT: 10192900) and \(\text{Fe}\) (with 99.9+\% purity purchased from Alfa Aesar (STOCK: 00170, LOT: J3OK28) powders into a DAC, then compressed the DAC to 13.8 GPa and performed in-situ laser-heating for a part of the mixture up to 1820(70) K. This run was carried out at the beamline 13-IDD of the Advanced Photon Source (APS), Argonne National Laboratory (Argonne, IL), with a wavelength of \(\lambda = 0.2952 \text{ Å}\), and a spot-size of \(3(\text{V}) \times 4(\text{H}) \text{ µm}^2\). Detector tilts and sample to detector distance were calibrated using a LaB\(_6\) standard. The laser heating process formed a few single-crystal grains along with some powder of \(\text{Fe}_4\text{O}_5\). Then, we compressed these samples up to \(\sim100\) GPa and collected both single-crystal (\(\omega\) rotation of \(-33^\circ\) to \(+36^\circ\) with 0.5\(^\circ\) steps) and powder diffraction data. Single-crystal diffraction processing was performed in the same manner described in Run 1, and using an orthoenstatite standard from the same batch.

We employed DACs with diamond anvil culet sizes of 300 and 150 \(\mu\text{m}\), respectively. Together with the sample in the same cell we loaded a ruby ball (for the first run) and a chip of gold (for the second run) that was used for pressure determination [6]. The DACs were filled with a Ne pressure-transmitting medium. At each pressure point we acquired the single-crystal X-ray diffraction images upon a continuous rotation of the cell with the sample around the vertical \(\omega\)-axis with a step of \(\Delta \omega = 0.5^\circ\) and an exposure time of \(t = 0.5\) s/frame. The diffraction data were collected by a Perkin Elmer XRD1621 detector at DESY and a Pilatus 1M CdTe detector at APS. We analyzed these data with CrysAlisPro software [7] and solved the crystal structures using JANA2006 software [8]. We note that the single-crystal data were obtained up to \(\sim94\) GPa and the images show that under pressure the structure does not change (see Figs. S2 and S3). However, at elevated pressures, particularly above 50 GPa, the quality of the SC data deteriorates. This could be due to two main reasons:

1) The crystal experiences more stress as the pressure medium becomes less hydrostatic.
2) Electronic or structural transitions often induce such lowering of the crystal quality [9], with
the quality possibly improving upon completion of the transition, as seen in this case at 93.9(14) GPa [Figs. S2 and S3]. Correspondingly the error estimates of the atomic positions and unit-cell parameters obtained above 50 GPa are large; accordingly we do not plot them. The powder diffraction data were first integrated using DIOPTAS [10] and then analyzed by LeBail extraction using GSAS II [11]. Powder XRD was used mainly for obtaining the lattice parameters and equations of state (EOS) at the whole pressure range. The pressure uncertainties are ∼0.3-1.5 GPa from low to high pressures. Due to the large number of overlapping peaks, the c axis values were fixed according to the position of the (002) peak, which is well separated from other peaks. The reported uncertainties are given according to the standard errors obtained from the respective software used for fitting the data.

**Structure solution and refinement of Fe₄O₅**

The crystal structure of Fe₄O₅ reported by Lavina et al. [12] (space group Cmcm, Z = 4) was used as a starting model for the refinement. Since a body of the diamond anvil cell shadows more than 50% of the diffraction reflections, the reflection datasets were incomplete. In order to improve the data/parameter ratio, we refined atomic thermal parameters in isotropic approximation. The structures were refined by full-matrix least squares against $F^2$ using the SHELXL-2014/7 [13] implemented in OLEX2 software [14]. The resulting $R_1$ values varied from 6.0 to 7.8%. The most intense residual electron density peaks were not exceeding 1.8 e/Å³ and were found within 1 Å of the Fe-atoms. The detailed summary of the crystal structure refinements along with information on unit cell parameters, atomic coordinates and isotropic displacement parameters are summarized in Tables S3–S5.

To evaluate the oxidation states of different Fe ions in the crystal structure we applied a bond-valence-sum (BVS) approach [15] based on the analysis of Fe–O bond lengths around the Fe ions. In this method the oxidation state of an ion $V_i$ is the sum of all its bond valences $S_{ij}$, each of which is determined as $S_{ij} = \exp((R_{ij} - d_{ij})/b_0)$, where $d_{ij}$ is the distance between atoms $i$ and $j$, $R_{ij}$ is the empirically determined distance for this cation–anion pair and $b_0$ is an empirical parameter, which is normally about 0.37 Å [15].
Electrical transport measurements

Electrical transport measurements up to 100 GPa were performed using TAU piston-cylinder DACs. A crystal with dimensions of about $70 \times 70 \times 20 \ \mu m$ was loaded into a cavity of $100 \ \mu m$ in diameter, drilled in a rhenium gasket. The gasket was insulated with a layer of $Al_2O_3$-NaCl (in the atomic ratio of 3:1) that was mixed with an epoxy. Some amount of a CaSO$_4$ powder was prepressed into the cavity before the crystal loading to ensure a quasi-hydrostatic environment around the sample. Six platinum triangles, which served as electrodes, were placed on the culet. This assembly permitted the measurements in various DC four-probe arrangements at a given pressure. The Pt electrodes were connected to exterior conducting wires with a silver epoxy. The electrical resistance was measured as a function of pressure and temperature (for both compression and decompression cycles) using the standard four-probe method in a custom-made cryostat. At each temperature point, the voltage was measured as a function of a series of applied electrical currents to determine the electrical resistance from a slope of their dependence. The temperature was measured using a Lakeshore Si (DT-421-HR) diode in proximity to the DAC. A few ruby pieces were placed in the central region of the culet between the Pt electrodes around the sample for determination of the pressure. The pressure inside the DAC was determined both before and after each measurement using the ruby $R_1$ fluorescence line as a pressure marker together with the calibration scales reported in Ref. [16]. The pressure gradients in the DAC were found to be rather insignificant. They amounted to $\sim$5% for the distances across which the voltage was measured ($15-20 \ \mu m$ between the tips of the Pt electrodes).

X-ray diffraction results

Our XRD experiments find the conservation of the original orthorhombic CaFe$_3$O$_5$-type structure up to $\sim$100 GPa (see Figs. S2-S5) but reveal a number of features in its compression behavior. Similar to [17], we find a steeper decrease of the unit-cell volume with pressure increase above $\sim$50 GPa, with $\Delta V/V \sim 2.4\%$. Above 56 GPa the volume variation becomes more gradual and shows only an additional tiny volume drop of $\sim$0.3% at about 84 GPa. Analyzing the $V(P)$ behavior we can highlight the existence of three pressure ranges, namely, from ambient pressure to about 50 GPa (labelled as LP phase), 56–81 GPa (HP1 phase),
and 84–100 GPa (HP2 phase) (see Table S1). As we show in the main text these pressure ranges correspond to different electronic states within the same crystal structure. The unit-cell volume data for these ranges can be fitted using the third- or second-order Birch-Murnaghan (BM3/BM2) equations of state (EOS) [18] (see Table S2). The fit of the $V(P)$ data was performed with the software EosFit GUI [19], using weights for both $P$ and $V$ (see Table S2).

We note a significant “softening” of the material beyond $\sim$50 GPa. Thus, the bulk modulus of Fe$_4$O$_5$ almost halved and $V_0$ increase by $\sim$8%, compared to the LP phase (see Table S2). Such a behavior contradicts with the anticipated hardening of the material after the volume collapse. Similar behavior was reported for PrFeO$_3$ [20], in which a transition in Fe ions to the LS state was not completed simultaneously with a sharp isostructural phase transition around 50 GPa and continued as a sluggish second-order HS-LS transition at higher pressures.

**Pressure-induced high axial anisotropy of Fe$_4$O$_5$**

We note an unusual compression behavior of the parameter $b$ leading to a high axial compression anisotropy of the LP phase (see Fig. S6). In the previous work [2], it was documented that for a single crystal of Fe$_4$O$_5$ the parameter $b$ has a negative thermal expansion. This anomalous behavior was tentatively addressed to an antiferromagnetic spin alignment along this axis, which can gain in the exchange energy upon a Fe-Fe distances increase [17, 21]. Such spin alignment may explain also the observed unusual axial anisotropy of the LP phase and indications of the reduced compressibility of the FeO6 octahedra comprising of the Fe2 sites. We note that the high axial anisotropy collapses concurrently with the partial spin transition at $\sim$55 GPa, tentatively as the result of a significant decrease of $T_N$ and $H_{hf}$ accompanying usually HS-LS transitions [22–27].

**Temperature dependencies of the electrical resistance of Fe$_4$O$_5$**

Up to about 86 GPa the temperature dependencies of the electrical resistance of Fe$_4$O$_5$ are semiconducting-like, exhibiting a negative $R(T)$ slope (Fig. 2a). The curve at different fixed pressures for certain temperature ranges can be well described by an expression as
follows \( \ln R = \ln R_0 + \frac{E_a}{k_B T} \), where \( k_B \) is the Boltzmann’s constant, \( E_a \) the electrical transport activation energy [see Fig. 3(a)].

We note that a high-pressure low-temperature phase diagram of \( \text{Fe}_4\text{O}_5 \) determined in a previous study [4] established the existence of novel charge-ordered phases at moderate high pressures up to 40 GPa. Hence, the temperature dependencies of the electrical resistance in this pressure range should correspond to a mixture of the room temperature and low-temperature partially charge-ordered phases. The \( \ln R(1/T) \) dependences for pressures 4.2, 10.7 and 16.5 GPa show a small kink around 240 K, which, according to the phase diagram is consistent with the transition from orthorhombic \( \text{Cmcn} \) to charge-ordered \( \text{Fe}_4\text{O}_5\)-III phase [4]. In addition, for 10.7 and 16.5 GPa some change of the \( \ln R(1/T) \) slope is observed around 130 K coinciding with the onset of \( \text{Fe}_4\text{O}_5\)-IV phase [4]. For 4.2 GPa the change is around 110 K coinciding with the transition to \( \text{Fe}_4\text{O}_5\)-II [4]. For \( P = 37.2 \) and 50 GPa there is only a slope change around 230 K and at 61.2 GPa no appreciable changes are observed in \( \ln R(1/T) \) behavior.

**Theoretical Methods**

We supplement our single-crystal (SC) and powder (PWD) synchrotron x-ray diffraction (XRD) and resistance measurements by the density functional theory+dynamical mean-field theory (DFT+DMFT) electronic structure calculations [28, 29]. We study the electronic structure, magnetic properties, and valence configurations of iron of paramagnetic \( \text{Fe}_4\text{O}_5 \) using the fully charge self-consistent DFT+DMFT method implemented within plane-wave pseudopotentials [25, 26]. By using DMFT it becomes possible to treat the effects of electronic correlations (e.g., local spin and charge fluctuations) on the electronic properties of strongly correlated electron materials near the Mott transition [22, 23, 25, 26, 28–30]. In our DFT+DMFT calculations we construct a basis set of atomic-centered symmetry-constrained Wannier functions for the partially occupied Fe 3\( d \) bands evaluated within DFT [31]. The DFT+DMFT calculations are performed in the local basis set determined by diagonalization of the corresponding Fe 3\( d \) occupation matrices. We used the continuous-time hybridization-expansion quantum Monte-Carlo (segment) algorithm to solve the realistic many-body problem [32]. The DFT+DMFT calculations are performed in the paramagnetic state at an electronic temperature of \( T_{el} \sim 770 \) K (our calculations at 580 K give quanti-
tively similar results). In DMFT we use the Hubbard interaction $U = 6$ eV and Hund’s exchange coupling $J = 0.89$ eV for the Fe 3$d$ states in accordance with previous estimates [22, 23, 25, 26]. The $U$ and $J$ values are assumed to remain constant upon variation of the lattice. The Coulomb interaction was treated in the density-density approximation, spin-orbit coupling was neglected.

The electronic structure and magnetic properties of Mott-Hubbard systems are known to depend sensitively on the choice of the Coulomb interaction [33, 34]. We therefore check different Hubbard $U$ values, to make our DFT+DMFT based conclusions robust. In particular, we performed DFT+DMFT calculations with a sufficiently smaller Hubbard parameter $U = 5$ eV (while using the same Hund’s coupling, $J = 0.89$ eV). The DFT+DMFT approach was implemented within the plane-wave pseudopotentials with the generalized gradient approximation in DFT. We employed the fully localized double-counting correction, evaluated from the self-consistently determined local occupancies, to account for the electronic interactions already described by DFT. The spectral functions were computed using the maximum entropy method. Further technical details about the method used can be found in Ref. [25, 26].

In our DFT+DMFT calculations we adopted the crystal structure parameters taken from SC-XRD at three distinct pressures, corresponding to three distinct electronic phases in the equation of states of room-temperature Fe$_4$O$_5$, at $\sim$39 GPa, 62 GPa, and 84 GPa. While at 62 and 84 GPa the quality of SC-XRD data were not sufficient to extract atomic positions (only the lattice parameters were determined), we used atomic positions (internal atomic coordinates) obtained at 46.8 GPa for the DFT+DMFT calculations at 62 and 84 GPa. We use the DFT+DMFT approach with three nonequivalent impurity sites in the unit-cell in order to treat electron correlations in the Fe 3$d$ bands of the crystallographically distinct Fe1 (with prismatic oxygen coordination) and Fe2 and Fe3 ions (with octahedral coordination) of the orthorhombic CaFe$_3$O$_5$-type structure with space group Cmcm. For the given phases, we computed the site and orbitally-resolved Fe 3$d$ spectral functions, performed analysis of oxidation state of Fe ions, evaluated local spin susceptibilities $\chi(\tau) = \langle \hat{m}_z(\tau)\hat{m}_z(0) \rangle$, instantaneous and fluctuating local magnetic moments, $M_{\text{loc}}$. The latter are evaluated as the imaginary-time average of local spin susceptibilities as $M_{\text{loc}} = (k_B T \int \chi(\tau) d\tau)^{1/2}$. Our results for the pressure-dependence of the site-resolved $\chi(\tau)$ of Fe$_4$O$_5$ are shown in Fig. S7.

In agreement with our resistance measurements our DFT+DMFT calculations predict an
activation type behavior of the temperature-dependent resistance below $\sim 84$ GPa. Above $\sim 84$ GPa it undergoes a site-selective Mott IMT associated with metallization of the octahedral Fe2 and Fe3 sites, while the prismatic Fe1 sites remain Mott localized; thus, above $\sim 84$ GPa our calculations predict metallization of Fe$_4$O$_5$, in agreement with experiment. Moreover, our results for an energy gap are compatible to that extracted from our resistance measurement (taking into account that the energy gap depends on the Hubbard $U$ value). In addition, both experiment and theory show a gradual decrease of an energy gap value under pressure (which is typical for the high-pressure behavior of the Mott-Hubbard systems).

To determine the valence state of iron, we computed the reduced density matrix of the Wannier Fe 3$d$ states within DMFT. The eigenvalues of the reduced Fe 3$d$ density matrix give a probability of observing different 3$d$ electron atomic configurations, i.e., the Fe 3$d$ electrons are seen fluctuating due to quantum and temperature effects between various atomic configurations (see Ref. [25, 26] for further details). We note that this quantum many-body Wannier basis set based definition of valence gives an upper estimate. Consistent with this, our analysis yields nearly “pure” (Wannier) Fe 2+ and 3+ configurations for the prismatic and octahedral iron sites in Fe$_4$O$_5$ at low pressures. At the same time, the valence configuration can be approximated as an integrated charge density inside atomic sphere with a given radius (in accordance with quantum chemical Bader’s charge analysis). This quantum-chemical estimate of the oxidation state is related to bond valence sum analysis [15], in which valence is characterized by the bond length and coordination of an atom (here, prismatic or octahedral oxygen coordination). It is known to give a lower bound estimate of the valence state and hence of charge disproportionation (see, e.g., Refs. [35–37]). We note that both estimates of the oxidation state of iron in Fe$_4$O$_5$ yield qualitatively consistent results, giving direct evidence for charge ordering in room-temperature Fe$_4$O$_5$. Moreover, the quantum-chemical estimate of charge disproportionation of Fe ions in Fe$_4$O$_5$ gives about 0.14 $\bar{e}$ charge difference (i.e., of $\sim 14\%$ of the ideal valence skipping). This value is consistent with previous estimates for the low-temperature charge-ordered phases of the mixed-valent oxides, such as Fe$_3$O$_4$, of $\sim 0.2$ [35–37], and high-pressure charge-disproportionated phase of Fe$_2$O$_3$, of $\sim 0.1-0.18$ [22, 23].

Overall, our results for the electronic and lattice properties of the $Cmcm$ phase of Fe$_4$O$_5$ agree well with experimental data and provide a microscopic understanding of the complex pressure-induced evolution of the electronic and magnetic properties of Fe$_4$O$_5$. In particu-
lar, we obtain that at low pressures and room temperature Fe$_4$O$_5$ is a narrow-gap correlated insulator with an orthorhombic CaFe$_3$O$_5$-type crystal structure characterized by a localized charge ordering behavior of the Fe $2+/3+$ cations with alternating arrangement of iron (010) planes occupied by Fe $2+/3+$ cations. This result is consistent with an activation type behavior of the temperature-dependent resistance for pressures below $\sim$86 GPa (below 298 K), implying the formation of the Verwey-type charge ordering in Fe$_4$O$_5$. Under pressure, Fe$_4$O$_5$ undergoes a series of complicated isostructural electronic and magnetic-state transformations (space group symmetry remains unchanged, $Cmcm$). First, a HS-LS transition sets in for a fraction of the octahedral Fe$^{2+}$ ions (only the Fe2 sites are involved) starting at $\sim$50 GPa, which is followed by the site-selective Mott insulator-to-metal phase transition with metallization of the octahedral Fe2 and Fe3 states and Fe $2+$ to $3+$ valence crossover at the prismatic Fe sites (above 84 GPa). Thus, above $\sim$86 GPa the octahedral Fe2 and Fe3 sites adopt the LS state and are metallic, while the prismatic Fe1 sites are in the HS state and are Mott insulating.

While the DFT+DMFT calculations of the electronic structure and structural phase stability of Fe$_4$O$_5$ are computationally very demanding, we perform more simplified spin-polarized DFT electronic structure calculations of the compressional behavior of Fe$_4$O$_5$. In DFT we use the generalised gradient approximation for the correlation exchange functional [38]. To this end, we adopt the crystal structure data of RT Fe$_4$O$_5$ taken by our single crystal XRD at 39 GPa and calculate the total energy of antiferromagnetically ordered state of Fe$_4$O$_5$ as a function of volume. While such calculations cannot explain the Mott insulating state and, hence, underestimate orbital ordering and charge ordering/disproportionation effects in Fe$_4$O$_5$, DFT predicts two consecutive pressure-induced HS-LS transitions at the octahedral Fe sites, first at Fe2 at $\sim$58 GPa and then at Fe3 above 80 GPa (see Figs. S8 and S9). At the same time, the prismatic Fe1 ions are in the HS state up to high pressure of $\sim$150 GPa. This result agrees well with the compressional behavior of Fe$_4$O$_5$ obtained by using the more sophisticated DFT+DMFT method. We note that DFT calculations predict a sizable decrease of the bulk modulus at $\sim$58 GPa from $K_0 = 172$ GPa for the LP phase to $\sim$140 GPa for the HP1 phase which is associated with the HS-LS crossover at the octahedral Fe2 sites, in agreement with our experimental results. The phase transition is accompanied by a volume collapse of $\sim$3.5%. Upon further compression, above $\sim$80 GPa our DFT calculations predict a HS-LS crossover at the octahedral Fe3 sites. It is accompanied by a reduction of
the unit-cell volume by $\sim 1.5\%$ and by a sizable *increase* of the bulk modulus from 140 GPa (in the HP1 phase) to $\sim 176$ GPa (in the HP2 phase). We note however that DFT calculations cannot properly explain a Fe$^{2+}$ to Fe$^{3+}$ valence crossover at the prismatic Fe1 sites at high pressure which is according to our DFT+DMFT results is related to the site-selective Mott IMT (metallization of the octahedral Fe2 and Fe3 sites, while the prismatic Fe1 sites remain Mott localized). This implies the crucial importance of the effects of strong electronic correlation, consistent with previous studies of the site-selective Mott IMT in Fe$_2$O$_3$ and $R$NiO$_3$ compounds.
FIG. S1: Crystal structure of Fe$_4$O$_5$ at ambient conditions.
FIG. S2: Single-crystal X-ray diffraction patterns of Fe$_4$O$_5$ at RT at various pressures. Reconstructed reciprocal lattice plane defined by [001] and [010] directions of a selected Fe$_4$O$_5$ grain at various pressures shown in the 1kl plane. Insets show an enlarged portion.
FIG. S3: Reconstructed reciprocal lattice plane defined by [001] and [100] directions of a selected Fe$_4$O$_5$ grain at various pressures shown in the $h0l$ plane.
FIG. S4: X-ray powder diffraction patterns of Fe$_4$O$_5$ at RT at various pressures ($\lambda = 0.2952$ Å).
FIG. S5: Refinement of XRD patterns collected at $T = 300$ K for Fe$_4$O$_5$ at 14.8 (a) and 73.6 GPa (b), respectively and the differences between the observed and calculated profiles. Marks show the calculated peak positions.
FIG. S6: Pressure dependencies of the relative unit-cell parameters, determined in the powder (a) and single crystal (b) X-ray diffraction studies. Note that parameters $a$ and $c$ show similar behavior and almost do not exhibit any peculiarities over the entire pressure range up to 100 GPa, except a small drop of the parameter $c$ at $\sim$84 GPa (see Fig. 1a). Meanwhile, the behavior of the parameter $b$ varies with pressure more dramatically: it shows a high stiffness and in the range of about 25–40 GPa it almost does not shrink under pressure. At higher pressures, the $b$ parameter shows a steeper decrease with pressure increase followed by a drop in the range of 53–56 GPa and only above 56 GPa it behaves similar to two other lattice parameters indicating the collapse of the axial anisotropy.
FIG. S7: Site-resolved local spin susceptibilities \( \chi(\tau) = \langle \hat{m}_z(\tau)\hat{m}_z(0) \rangle \) of paramagnetic Fe\(_4\)O\(_5\) as obtained by DFT+DMFT for different pressures.
FIG. S8: Compressional behavior of Fe₄O₅ obtained by spin-polarized DFT total-energy calculations: the DFT total-energy results (a) and the obtained equation of states in comparison to XRD data (b). In (a) the DFT total-energy results are depicted by black squares. Our DFT results for two consecutive HS-LS transitions at the octahedral Fe₂ (at $V \sim 488.3$ a.u.$^3$, at $\sim 58$ GPa) and Fe₃ ions (at $V \sim 445.8$ a.u.$^3$, at $\sim 80$ GPa) and the corresponding collapse of the lattice volume of 3.5% and 1.5%, respectively, are shown with red shadings. Different colors depict different sets of EOS data. In (b) the XRD $V$-$P$ data points are shown by black squares.
FIG. S9: Compressional behavior of magnetic moments of the prismatic Fe1 and octahedral Fe2 and Fe3 ions as obtained by spin-polarized DFT calculations. Our DFT results for two consecutive HS-LS transitions at the octahedral Fe2 (at $V \sim 488.3$ a.u.$^3$, at $\sim$58 GPa) and Fe3 ions (at $V \sim 445.8$ a.u.$^3$, at $\sim$80 GPa) and the corresponding collapse of the lattice volume of 3.5% and 1.5%, respectively, are shown by red rectangles.
Table S1: The refined unit-cell volume of the Cmcm phase of Fe₄O₅ at various pressures. The uncertainties in the unit-cell volume are solely from the GSAS fitting output. Notes: the data points at the LP-HP1 transition range between 50 and 56 GPa were not used in any of the EOSs. For the LP EOS region we also used the ESRF single crystal data (except the point at 46.8 GPa). The $R_{wp}$ is the weighted-profile $R$-factor: $R_{wp} = \sqrt{\frac{\sum w_i (y_i(\text{obs}) - y_i(\text{calc}))^2}{\sum w_i (y_i(\text{obs}))^2}}$.

| EOS | $P$ (GPa) | $V$ (Å³) | $R_{wp}$ (%) |
|-----|----------|---------|-------------|
| LP  | 14.8(3)  | 333.15(9) | 0.90        |
| LP  | 16.1(3)  | 330.97(9) | 0.85        |
| LP  | 17.5(4)  | 329.56(8) | 0.75        |
| LP  | 19.3(4)  | 326.83(9) | 0.78        |
| LP  | 22.2(4)  | 323.79(7) | 0.62        |
| LP  | 23.8(4)  | 321.56(8) | 0.59        |
| LP  | 26.9(4)  | 319.36(10)| 0.66        |
| LP  | 28.9(4)  | 316.54(14)| 0.90        |
| LP  | 31.1(4)  | 314.33(13)| 0.84        |
| LP  | 32.9(6)  | 312.92(17)| 0.83        |
| LP  | 35.3(4)  | 311.31(18)| 0.86        |
| LP  | 36.7(4)  | 309.76(18)| 0.80        |
| LP  | 39.2(4)  | 307.60(22)| 0.84        |
| LP  | 41.1(5)  | 304.84(17)| 0.63        |
| LP  | 44.1(6)  | 303.00(16)| 0.58        |
| LP  | 47.0(6)  | 302.15(20)| 0.71        |
|     | 50.2(6)  | 296.87(26)| 0.86        |
|     | 53.5(6)  | 293.54(25)| 0.73        |
| HP1 | 56.6(6)  | 284.88(29)| 0.73        |
| HP1 | 59.0(7)  | 282.90(28)| 0.76        |
| HP1 | 62.0(7)  | 279.77(21)| 0.60        |
| HP1 | 65.1(7)  | 277.28(16)| 0.47        |
| HP1 | 67.9(7)  | 274.75(14)| 0.42        |
| HP1 | 71.2(7)  | 272.53(12)| 0.35        |
| HP1 | 74.0(8)  | 270.93(14)| 0.38        |
| HP1 | 76.1(8)  | 268.01(19)| 0.53        |
| HP1 | 78.4(8)  | 266.94(15)| 0.37        |
| HP1 | 80.9(12) | 265.39(21)| 0.45        |
| HP2 | 84.2(10) | 262.04(50)| 0.63        |
| HP2 | 85.1(10) | 260.77(30)| 0.47        |
| HP2 | 88.2(10) | 260.43(32)| 0.45        |
| HP2 | 90.2(12) | 258.08(40)| 0.59        |
| HP2 | 93.9(14) | 258.01(49)| 0.85        |
| HP2 | 95.6(12) | 254.77(37)| 0.61        |
| HP2 | 98.4(12) | 254.62(45)| 0.61        |
Table S2: Birch-Murnaghan EOS for the various phases of Fe₄O₅. (K₀, K' and V₀ are the bulk modulus, its pressure derivative, and the unit-cell volume (at 1 bar and 300 K), respectively; K₅₀ and K₈₄ are the bulk modulus at 50 and 84 GPa, correspondingly). We note that the values obtained for LP phase are in good agreement with previous data [7,9,10].

| Phase         | EOS | V₀, Å³ | K₀, GPa | K₅₀, GPa | K₈₄, GPa | K'   |
|---------------|-----|--------|---------|----------|----------|------|
| LP phase, 0 – 50 GPa | BM3 | 356.88(3) | 175(3)  | 417(3)   | 5.4(3)   |
| LP phase, 0 – 50 GPa | BM2 | 356.86(5) | 190.2(11) | 375(1)   | 4        |
| HP1 phase, 56 – 81 GPa | BM2 | 386(7)    | 102(9)  | 279(3)   | 388(11)  | 4    |
| HP1 phase, 56 – 81 GPa | BM3 | 370(60)   | 150(200) | 293(8)   | 371(8)   | 3(3) |
| HP2 phase, 84 – 100 GPa | BM2 | 360(26)   | 140(40) | 430(60)  | 4        |
Table S3. Details of crystal structure refinements for Fe₄O₅ at high pressures* (ESRF)

| Pressure, GPa | 0.0001 | 10.1(5) | 14.4(5) | 18.2(5) | 22.4(5) | 25.6(5) | 30.4(5) | 31.7(5) | 46.8(5) |
|--------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| $a$ (Å)      | 2.89510(13) | 2.83673(19) | 2.8176(2) | 2.8012(4) | 2.7785(4) | 2.7726(6) | 2.7554(7) | 2.7601(6) | 2.7158(5) |
| $b$ (Å)      | 9.8054(6) | 9.6803(8) | 9.6494(10) | 9.6307(15) | 9.6029(15) | 9.607(2) | 9.568(3) | 9.589(3) | 9.3216(18) |
| $c$ (Å)      | 12.576(9) | 12.366(15) | 12.263(16) | 12.16(2) | 12.10(2) | 12.00(3) | 11.95(4) | 11.84(4) | 11.81(3) |
| $V$ (Å³)    | 357.0(3) | 339.6(4) | 333.4(4) | 327.9(6) | 322.9(6) | 319.6(9) | 315.1(10) | 313.5(10) | 298.9(7) |
| Reflections collected | 416 | 382 | 403 | 355 | 384 | 294 | 283 | 348 | 305 |
| Independent reflections | 79 | 80 | 77 | 77 | 76 | 76 | 71 | 77 | 67 |
| Independent reflections [$I > 2\sigma(I)$] | 75 | 74 | 73 | 75 | 71 | 70 | 64 | 71 | 58 |
| Refined parameters | 15 | 15 | 15 | 15 | 15 | 15 | 15 | 15 | 15 |
| $R_{int}(F^2)$ | 0.0409 | 0.0439 | 0.0481 | 0.0422 | 0.04 | 0.0364 | 0.0684 | 0.0597 | 0.0699 |
| $R(\sigma)$ | 0.0215 | 0.0375 | 0.0219 | 0.0175 | 0.0193 | 0.0179 | 0.0485 | 0.0337 | 0.0501 |
| $R_1 [I > 2\sigma(I)]$ | 0.0651 | 0.06 | 0.0563 | 0.0711 | 0.0775 | 0.0717 | 0.0625 | 0.0755 | 0.0743 |
| $wR_2 [I > 2\sigma(I)]$ | 0.1702 | 0.15 | 0.1603 | 0.1898 | 0.189 | 0.163 | 0.1682 | 0.1884 | 0.1921 |
| $R_1$ | 0.0658 | 0.0617 | 0.0571 | 0.0719 | 0.0794 | 0.0742 | 0.0666 | 0.0783 | 0.0777 |
| $wR_2$ | 0.1743 | 0.1571 | 0.1664 | 0.1913 | 0.1984 | 0.1701 | 0.1723 | 0.1912 | 0.1977 |
| Goodness of fit on $F^2$ | 1.161 | 1.218 | 1.212 | 1.211 | 1.139 | 1.115 | 1.208 | 1.138 | 1.126 |
| $\Delta\rho_{\text{max}}(\epsilon / \text{Å}^3)$ | 1.487 | 1.235 | 0.732 | 1.187 | 1.797 | 1.268 | 0.866 | 1.199 | 1.169 |
| $\Delta\rho_{\text{min}}(\epsilon / \text{Å}^3)$ | -1.416 | -1.243 | -1.418 | -1.474 | -1.556 | -1.083 | -0.89 | -1.434 | -1.142 |
Table S4. Structural data for Fe₄O₅ at high pressures* (ESRF)

| Pressure, GPa | 0.0001 | 10.1(5) | 14.4(5) | 18.2(5) | 22.4(5) | 25.6(5) | 30.4(5) | 31.7(5) | 46.8(5) |
|--------------|--------|---------|---------|---------|---------|---------|---------|---------|---------|
| \(y\) (Fe1)  | 0.5054(3) | 0.5038(3) | 0.5039(3) | 0.5047(4) | 0.5051(3) | 0.5058(3) | 0.5069(4) | 0.5075(4) | 0.5092(4) |
| \(y\) (Fe3)  | 0.26023(17) | 0.26144(18) | 0.2620(2) | 0.2627(2) | 0.2631(2) | 0.26352(19) | 0.2643(3) | 0.2647(3) | 0.2659(3) |
| \(z\) (Fe3)  | 0.1182(3) | 0.1179(4) | 0.1182(4) | 0.1178(6) | 0.1185(5) | 0.1181(5) | 0.1177(8) | 0.1182(7) | 0.1185(7) |
| \(y\) (O1)   | 0.1593(13) | 0.1588(15) | 0.1582(16) | 0.1598(19) | 0.1606(19) | 0.1592(15) | 0.1577(16) | 0.1618(16) | 0.161(2) |
| \(y\) (O2)   | 0.3580(8) | 0.3579(9) | 0.3569(9) | 0.3582(12) | 0.3569(12) | 0.3593(9) | 0.3578(13) | 0.3553(13) | 0.3639(12) |
| \(z\) (O2)   | 0.543(2) | 0.546(2) | 0.543(3) | 0.545(3) | 0.547(3) | 0.549(3) | 0.543(3) | 0.546(3) | 0.548(4) |
| \(y\) (O3)   | 0.0929(9) | 0.0899(10) | 0.0891(11) | 0.0887(13) | 0.0857(14) | 0.0883(12) | 0.0866(14) | 0.0856(14) | 0.0851(17) |
| \(z\) (O3)   | 0.6416(16) | 0.6429(19) | 0.6430(18) | 0.643(3) | 0.646(2) | 0.647(2) | 0.649(3) | 0.647(2) | 0.650(3) |
| \(U_{\text{iso}}\) (Fe1) (\(\text{Å}^2\)) | 0.0084(10) | 0.0071(9) | 0.0088(10) | 0.0080(11) | 0.0132(12) | 0.0110(10) | 0.0112(12) | 0.0097(12) | 0.0216(14) |
| \(U_{\text{iso}}\) (Fe2) (\(\text{Å}^2\)) | 0.0088(10) | 0.0086(9) | 0.0103(10) | 0.0099(12) | 0.0152(12) | 0.0118(11) | 0.0131(12) | 0.0121(12) | 0.0262(14) |
| \(U_{\text{iso}}\) (Fe3) (\(\text{Å}^2\)) | 0.0077(9) | 0.0074(8) | 0.0092(9) | 0.0086(11) | 0.0140(11) | 0.0115(10) | 0.0116(11) | 0.0110(11) | 0.0244(13) |
| \(U_{\text{iso}}\) (O1) (\(\text{Å}^2\)) | 0.010(2) | 0.010(2) | 0.012(3) | 0.009(3) | 0.015(3) | 0.008(2) | 0.007(3) | 0.005(3) | 0.018(3) |
| \(U_{\text{iso}}\) (O2) (\(\text{Å}^2\)) | 0.011(2) | 0.010(2) | 0.013(2) | 0.011(3) | 0.018(3) | 0.011(2) | 0.010(2) | 0.009(2) | 0.020(3) |
| \(U_{\text{iso}}\) (O3) (\(\text{Å}^2\)) | 0.0104(18) | 0.0082(19) | 0.0091(19) | 0.007(2) | 0.015(2) | 0.010(2) | 0.009(2) | 0.007(2) | 0.020(2) |

*atoms' Wyckoff positions:
Fe1 4c (0, \(y\), 0.25)
Fe2 4a (0, 0, 0)
Fe3 8f (0, \(y\), \(z\))
O1 4c (0, \(y\), 0.25)
O2 8f (0, \(y\), \(z\))
O3 8f (0, \(y\), \(z\))
### Table S5. Interatomic distances in FeO₆ polyhedra in Fe₄O₅ (ESRF)

| Pressure, GPa | 0.0001 | 10.1(5) | 14.4(5) | 18.2(5) | 22.4(5) | 25.6(5) | 30.4(5) | 31.7(5) | 46.8(5) |
|--------------|--------|---------|---------|---------|---------|---------|---------|---------|---------|
| $d(\text{Fe}1-\text{O}1)$ x₂ (Å) | 2.091(9) | 2.064(11) | 2.049(11) | 2.047(14) | 2.040(14) | 2.023(11) | 1.995(11) | 2.023(11) | 1.960(15) |
| $d(\text{Fe}1-\text{O}3)$ x₄ (Å) | 2.210(13) | 2.142(14) | 2.124(14) | 2.11(2) | 2.087(19) | 2.066(15) | 2.035(19) | 2.047(18) | 2.004(18) |
| $d(\text{Fe}2-\text{O}2)$ x₄ (Å) | 2.079(8) | 2.055(9) | 2.043(10) | 2.032(13) | 2.035(13) | 2.023(11) | 2.004(12) | 2.031(12) | 1.942(14) |
| $d(\text{Fe}2-\text{O}3)$ x₂ (Å) | 2.000(19) | 1.97(2) | 1.95(2) | 1.93(3) | 1.92(3) | 1.96(2) | 1.97(3) | 1.92(3) | 1.94(3) |
| $d(\text{Fe}3-\text{O}1)$ (Å) | 1.930(7) | 1.912(9) | 1.902(9) | 1.888(12) | 1.871(11) | 1.873(10) | 1.882(13) | 1.847(12) | 1.835(14) |
| $d(\text{Fe}3-\text{O}2)$ (Å) | 2.24(2) | 2.23(3) | 2.18(3) | 2.18(4) | 2.20(4) | 2.20(3) | 2.12(3) | 2.13(3) | 2.16(4) |
| $d(\text{Fe}3-\text{O}2)$ x₂ (Å) | 2.084(11) | 2.035(13) | 2.036(15) | 2.024(19) | 2.002(19) | 2.002(14) | 2.014(18) | 1.991(18) | 2.00(2) |
| $d(\text{Fe}3-\text{O}3)$ x₂ (Å) | 2.063(7) | 2.044(8) | 2.035(8) | 2.025(10) | 2.033(11) | 2.017(9) | 2.019(10) | 2.020(10) | 1.977(12) |
Table S6. Details of crystal structure refinements for Fe₄O₅ at high pressures* (APS)

| Pressure, GPa | 14.8(3) | 17.5(4) | 22.2(4) | 26.9(4) | 31.1(4) | 35.3(4) | 39.2(4) | 44.1(6) | 56.6(6) |
|--------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| a (Å)        | 2.8282(4)| 2.8138(5)| 2.7994(4)| 2.7872(5)| 2.7779(7)| 2.7632(11)| 2.7642(11)| 2.7396(12)| 2.740(3) |
| b (Å)        | 9.639(5) | 9.608(6) | 9.572(9) | 9.487(10)| 9.368(13)| 9.35(2)  | 9.45(3)  | 9.31(7)  | 9.077(14)|
| c (Å)        | 12.266(2)| 12.204(2)| 12.128(3)| 12.064(3)| 12.015(4)| 11.951(5)| 11.93(2) | 11.45(3) | 9.31(7)  |
| V (Å³)       | 334.39(19)| 329.9(2) | 325.0(3) | 319.0(4) | 312.7(5) | 308.7(7) | 308.8(7) | 306.8(10)| 300(2)  | 283.1(6)|
| Reflections collected | 480 | 413 | 456 | 404 | 443 | 423 | 429 | 419 | 315 | 263 |
| Independent reflections | 179 | 150 | 234 | 216 | 211 | 123 | 127 | 120 | 44 | 60 |
| Independent reflections [I > 2σ(I)] | 232 | 222 | 169 | 153 | 169 | 156 | 160 | 153 | 115 | 90 |
| Rint(F²)     | 0.008   | 0.0125  | 0.0207  | 0.0145  | 0.0198  | 0.029   | 0.0293  | 0.0383  | 0.1266  | 0.0813 |
| R(σ)         | 0.0093  | 0.0134  | 0.0167  | 0.0154  | 0.0155  | 0.0374  | 0.0355  | 0.042   | 0.094   | 0.0378 |
| R₁ [I > 2σ(I)] | 0.0394 | 0.0378 | 0.0475 | 0.0478 | 0.0485 | 0.0692 | 0.0655 | 0.0727 | 0.1499 | 0.1055 |
| wR₂ [I > 2σ(I)] | 0.0488 | 0.0452 | 0.0536 | 0.0591 | 0.0552 | 0.0765 | 0.0702 | 0.0792 | 0.1607 | 0.1096 |
| R₁           | 0.0484  | 0.0471  | 0.0522  | 0.0534  | 0.0582  | 0.0832  | 0.0784  | 0.1027  | 0.2395  | 0.1348 |
| wR₂          | 0.0497  | 0.0459  | 0.0539  | 0.0596  | 0.056   | 0.0781  | 0.072   | 0.0815  | 0.186   | 0.1112 |
| Goodness of fit on F² | 3 | 2.49 | 2.89 | 3.29 | 3.12 | 2.98 | 2.57 | 3.05 | 3.1 | 2.99 |
| Δρmax(e / Å³) | 1.1 | 1 | 1.17 | 1.39 | 2.32 | 2.26 | 1.95 | 2.4 | 3.91 | 1.54 |
| Δρmin(e / Å³) | -1.33 | -1.18 | -1.73 | -1.38 | -1.46 | -1.63 | -1.47 | -1.49 | -3.91 | -1.9 |
Table S7. Structural data for Fe₄O₅ at high pressures* (APS)

| Pressure, GPa | 14.8(3) | 17.5(4) | 22.2(4) | 26.9(4) | 31.1(4) | 35.3(4) | 39.2(4) | 44.1(6) | 56.6(6) |
|--------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| y (Fe1)      | 0.5033(2)| 0.5037(2)| 0.5040(4)| 0.5055(4)| 0.5060(4)| 0.5062(6)| 0.5056(6)| 0.5063(8)| 0.508(4)| 0.527(2) |
| y (Fe3)      | 0.26186(15)| 0.26227(14)| 0.2632(2)| 0.2647(3)| 0.2650(4)| 0.2645(4)| 0.2658(5)| 0.265(2)| 0.2775(13)|
| z (Fe3)      | 0.1179(6)| 0.11797(7)| 0.11782(10)| 0.11790(11)| 0.11784(11)| 0.11790(17)| 0.1177(2)| 0.1185(7)| 0.1093(4)|
| y (O1)       | 0.1550(12)| 0.1565(10)| 0.1555(17)| 0.1590(19)| 0.1591(18)| 0.161(3)| 0.163(3)| 0.157(4)| 0.139(17)| 0.207(11)|
| y (O2)       | 0.3600(9)| 0.3574(7)| 0.3582(12)| 0.3572(14)| 0.3580(13)| 0.358(2)| 0.357(2)| 0.355(2)| 0.342(10)| 0.353(9)|
| z (O2)       | 0.5443(3)| 0.5445(4)| 0.5442(5)| 0.5440(6)| 0.5447(5)| 0.5446(8)| 0.5461(8)| 0.5454(10)| 0.549(4)| 0.547(3)|
| y (O3)       | 0.0917(8)| 0.0898(7)| 0.0888(12)| 0.0895(13)| 0.0870(13)| 0.086(2)| 0.0894(19)| 0.084(2)| 0.091(7)| 0.067(5)|
| z (O3)       | 0.6445(3)| 0.6445(3)| 0.6452(5)| 0.6456(5)| 0.6464(5)| 0.6470(7)| 0.6474(7)| 0.6474(10)| 0.647(2)| 0.648(2)|
| U_{iso}(Fe1) (Å²) | 0.0084(3)| 0.0073(3)| 0.0071(4)| 0.0105(5)| 0.0097(5)| 0.0127(7)| 0.0122(7)| 0.0134(8)| 0.037(4)| 0.032(3)|
| U_{iso}(Fe2) (Å²) | 0.0092(3)| 0.0086(3)| 0.0082(5)| 0.0118(5)| 0.0112(5)| 0.0140(7)| 0.0144(7)| 0.0150(9)| 0.018(3)| 0.025(2)|
| U_{iso}(Fe3) (Å²) | 0.0088(3)| 0.0081(3)| 0.0078(4)| 0.0114(4)| 0.0106(4)| 0.0140(6)| 0.0137(6)| 0.0146(7)| 0.019(2)| 0.029(2)|
| U_{iso}(O1) (Å²) | 0.0081(11)| 0.0087(12)| 0.0061(16)| 0.0102(17)| 0.0080(17)| 0.011(2)| 0.011(2)| 0.015(3)| 0.036(17)| 0.038(11)|
| U_{iso}(O2) (Å²) | 0.0093(8)| 0.0080(8)| 0.0078(11)| 0.0115(12)| 0.0101(12)| 0.0135(18)| 0.0125(19)| 0.013(2)| 0.028(11)| 0.043(8)|
| U_{iso}(O3) (Å²) | 0.0075(8)| 0.0078(8)| 0.0071(11)| 0.0086(12)| 0.0098(12)| 0.0103(17)| 0.0082(16)| 0.012(2)| 0.005(6)| 0.023(7)|

*atoms' Wyckoff positions:
Fe1 4c (0, y, 0.25)
Fe2 4a (0, 0, 0)
Fe3 8f (0, y, z)
O1 4c (0, y, 0.25)
O2 8f (0, y, z)
O3 8f (0, y, z)
Table S8. Interatomic distances in FeO6 polyhedra in Fe4O5 (APS)

| Pressure, GPa | 14.8(3) | 17.5(4) | 22.2(4) | 26.9(4) | 31.1(4) | 35.3(4) | 39.2(4) | 44.1(6) | 56.6(6) |
|--------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| \(d(Fe1-O1)\) \(x2\) (Å) | 2.034(8) | 2.033(7) | 2.016(12) | 2.015(14) | 1.997(13) | 2.002(19) | 2.02(2) | 1.98(3) | 1.83(11) | 2.12(8) |
| \(d(Fe1-O3)\) \(x4\) (Å) | 2.124(4) | 2.108(4) | 2.089(6) | 2.083(7) | 2.058(7) | 2.042(10) | 2.05(10) | 2.022(13) | 2.05(4) | 1.98(3) |
| \(d(Fe2-O2)\) \(x4\) (Å) | 2.029(6) | 2.037(5) | 2.022(8) | 2.015(9) | 1.996(9) | 1.986(13) | 1.998(14) | 2.008(17) | 1.99(7) | 1.97(6) |
| \(d(Fe2-O3)\) \(x2\) (Å) | 1.981(5) | 1.963(5) | 1.956(7) | 1.951(8) | 1.939(8) | 1.933(11) | 1.950(11) | 1.920(15) | 1.93(4) | 1.83(3) |
| \(d(Fe3-O1)\) (Å) | 1.920(6) | 1.905(5) | 1.906(9) | 1.878(10) | 1.871(9) | 1.853(14) | 1.842(14) | 1.87(2) | 1.94(10) | 1.76(4) |
| \(d(Fe3-O2)\) (Å) | 2.203(5) | 2.183(5) | 2.165(8) | 2.145(8) | 2.139(8) | 2.129(12) | 2.143(12) | 2.111(15) | 2.15(6) | 1.94(4) |
| \(d(Fe3-O2)\) \(x2\) (Å) | 2.048(5) | 2.026(4) | 2.026(7) | 2.013(8) | 2.006(8) | 2.002(12) | 1.985(12) | 1.980(15) | 1.96(6) | 1.93(5) |
| \(d(Fe3-O3)\) \(x2\) (Å) | 2.025(5) | 2.026(5) | 2.019(8) | 1.998(9) | 1.994(9) | 1.991(14) | 1.975(13) | 2.001(18) | 1.95(5) | 2.00(4) |
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