MHD Double-Diffusive Carreau Fluid Flow through a Porous Medium with Variable Thermal Conductivity and Suction/Injection

Salman Zeb 1, Shafiq Ahmad 1, Muhammad Ibrahim 2,3,* and Tareq Saeed 3

Department of Mathematics, University of Malakand, Chakdara 18800, Dir (Lower), Khyber Pakhtunkhwa, Pakistan; salmanzeb@uom.edu.pk (S.Z.); shafiq49043@gmail.com (S.A.)

Department of Basic Sciences, CECOS University of IT and Emerging Sciences, Peshawar 25000, Pakistan

Nonlinear Analysis and Applied Mathematics (NAAM)-Research Group, Department of Mathematics, Faculty of Science, King Abdulaziz University, P.O. Box 80203, Jeddah 21589, Saudi Arabia; tsalmalki@kau.edu.sa

* Correspondence: muhammad.ibrahim@cecos.edu.pk

Abstract: In this article, we consider the effects of double diffusion on magnetohydrodynamics (MHD) Carreau fluid flow through a porous medium along a stretching sheet. Variable thermal conductivity and suction/injection parameter effects are also taken into the consideration. Similarity transformations are utilized to transform the equations governing the Carreau fluid flow model to dimensionless non-linear ordinary differential equations. Maple software is utilized for the numerical solution. These solutions are then presented through graphs. The velocity, concentration, temperature profile, skin friction coefficient, and the Nusselt and Sherwood numbers under the impact of different parameters are studied. The fluid flow is analyzed for both suction and injection cases. From the analysis carried out, it is observed that the velocity profile reduces by increasing the porosity parameter while it enhances both the temperature and concentration profile. The temperature field enhances with increasing the variable thermal conductivity and the Nusselt number exhibits opposite behavior.

Keywords: variable thermal conductivity; Carreau fluid; double diffusion; magnetic field; porous medium; suction and injection

1. Introduction

Non-Newtonian fluids have gained great attention due to their immense applications in industrial and biomedical applications. The study concerning electrically conducting non-Newtonian fluids passing through a stretching sheet has been done by many researchers due to its vast engineering and industrial applications comprising plastic and metal extrusion, insulating materials, metal spinning, and in insulating materials. Sahoo [1] studied the non-Newtonian fluids past a stretched sheet while considering partial slip. It was found that the slip diminishes the momentum boundary layer thickness while enhancing the thermal boundary layer. Akbar et al. [2] explained the magnetohydrodynamics (MHD) flow of the tangent hyperbolic fluid through a stretching surface. They concluded that the velocity exhibits a decreasing behavior due to augmentation in magnetic parameter, power index, and the Weisssenber number. Hamid et al. [3] found the dual solution and performed an analysis of heat transport and flow of the MHD Casson fluid towards an expanding sheet. The results showed that the fluid gives steady profiles for positive eigenvalues. Sharma and Bisht [4] studied MHD Sisko nanofluid along with joule heating through a stretching sheet. The results revealed that with joule heating, the velocity profile reduces whereas the temperature increases significantly. Salahuddin et al. [5] studied the MHD flux of the Williamson fluid towards a stretching sheet under the Catteneo–Christov
heat flow model with varying thickness. Their results showed that the impact of the magnetic parameter is opposite on the velocity whereas temperature enhances due to an increase in the magnetic parameter. Additionally, greater values for the wall thickness were considered suitable for the reduction in the velocity profile. Zakir et al. [6] studied MHD tangent hyperbolic fluid slip flow through stretching sheet. For further study related to fluid flow problems through a stretching sheet we refer to [7–12].

Double diffusion in fluid flow is a phenomenon that discusses a type of convection with two different density gradients both having different diffusive rates. This is a very important phenomenon and many researchers are driven to study it. Malik et al. [13] analyzed Sisko fluid under the Cattaneo–Christov double-diffusive model. It is deducted that with great relaxation times the temperature, as well as the concentration profiles, reduce. Waqas et al. [14] studied a chemically reactive non-Newtonian fluid with improved double diffusion. The concentration profile increases more for the destructive chemical reaction parameter than the generative parameter. Haq et al. [15] discussed stagnation point flux with the magnetic field, thermal radiation, and slip effect towards an expanding sheet and the results revealed that temperature elevates with increasing thermophoresis parameter while, due to the Brownian motion, the concentration profile reduces. Shankaralingappa [16] discussed double-diffusive Oldroyd-B fluid flow along a stretch sheet while utilizing Cattaneo–Christov heat theory in addition to the consideration of thermophoretic particle deposition, heat source/sink, and relaxation chemical reaction. Their results showed that velocity profile declines for rotation parameter and temperature and concentration profiles decline for increasing relaxation time parameter, and the concentration distribution reduces for enhancing values of chemical reaction rate and thermophoretic parameter. Kumar et al. [17] analyzed viscous ferromagnetic liquid flow along a stretched cylinder having thermophoretic particle deposition and with a uniform heat source/sink. Their outcomes described that the velocity field reduces when enhancing the thermophoretic coefficient and parameter, and the thermal gradient enhances when raising the ferromagnetic interaction parameter, while the opposite behavior is seen for the heat source/sink parameter.

Fluid flow via a porous medium has a significant amount of applications in petroleum engineering, geothermal and industrial operations. A porous medium is a solid matrix having a continuous network of pores. A porous medium which allows fluid flow can be natural including sand, wood, and human lungs or it can be synthetic such as ceramics, metal foams having high porosity, and composite materials. Pores and interconnected solid particles make up porous media which can be seen in electrochemical systems, steel and iron production, microchemical reactors, and renewable fuels. Traditionally, Darcy’s law is utilized mainly for computational and theoretical investigations of porous medium studies. Heat transfer effects and fluid flow through a porous medium are studied by numerous researchers. Khan et al. [18] studied triple diffusive flow saturated by nanofluid through a permeable horizontal plate and showed that heat transfer rate enhances with adding nano-particles and salts. Krishna and Reddy [19] discussed the MHD non-Newtonian forced convective flow via porous medium through a stumpy and deduced that heat transfer is dominated at low porosity by conduction while for high porosity it is dominated by convection. Hayat et al. [20] carried out the analysis on MHD slip flux and heat transport effects over a penetrable stretching sheet. Siavashi and Rostami [21] studied non-Newtonian nanofluid with natural convective properties along a concentric circular region with completely or partially filled porous medium. They considered the two phase simulations of the fluid and the results disclosed that a fully porous cavity generates less entropy because in the porous zone the fluid has the lowest temperature gradients. Eldabe et al. [22] discussed the viscous dissolution effect on the free convection flux via porous media.

The Carreau fluid flow model is a significant non-Newtonian fluid model. It effectively describes both shear thickening and shear thinning phenomena. At a high wall shear stress, the behavior of this fluid degenerates to a Newtonian behavior. This model considerably explains the rheological behavior of many industrial fluids such as foams, cosmetics, syrups,
and biotechnological detergents. Khan et al. [23] discussed the effects of heat transfer of squeezed Carreau fluid passing through a sensor area with changing thermal conductivity. Velocity increases with both enlarging the permeable velocity and the squeezed flow parameter. A study of the heat and mass transport impacts of radiative Carreau fluid with a magnetic field is presented by Machireddy and Naramgari [24]. Sulochana et al. [25] explained the transpiration impact of Carreau nanofluid with stagnation-point flow amid Brownian motion and thermophoresis. The study explains that the heat and mass transport rates elevate with the thermophoresis parameter. The impact of solar radiation and heat generation on Carreau nanofluid with varying thickness passing across a stretched sheet is studied by Khan et al. [26]. Velocity enhances with wall thickness parameter, and heat generation and radiative heat parameter cause an increase in temperature. Raju and Sandeep [27] studied MHD Carreau fluid across a wedge having the effects of cross-diffusion and found that decelerating flow past a wedge is good for cooling. Non-Newtonian MHD Carreau fluid in a sphere is investigated numerically by Amanulla et al. [28]. Akbar et al. [29] studied peristaltic flux of Carreau nanofluid through an uneven channel. Pressure rise enhances with the magnetic and thermophoresis parameters. The authors in [30] investigated MHD Carreau fluid flow along a variable stretch sheet and found that velocity field declines for enhancing power-law index and magnetic parameter values.

In this article, we examine MHD Carreau fluid flow in permeable media over a stretched sheet. Double diffusion, variable thermal conductivity, and Darcy’s law are employed for porous medium in the modeling of the problem. Equations governing the considered Carreau fluid flow model problem are transformed to non-linear ordinary differential equations in dimensionless form by employing similarity transformations. The effects of pertinent parameters present in the problem for injection/suction cases on velocity, temperature, concentration, and on other physical quantities such as skin friction and Nusselt and Sherwood numbers are investigated, represented graphically, and discussed accordingly.

The remaining article is organized as follows: The problem formulation is presented in Section 2. In Section 3, we analyzed our results, while the conclusion of the work is given in Section 4.

2. Problem Formulation

We consider steady incompressible flow of a double diffusive Carreau fluid through porous medium over a stretching sheet in two dimensions. Assuming that the sheet is considered in the $x$ direction with stretching velocity $u_w = ax$, where $a > 0$ is a constant and is the stretching rate. The flow is restricted to the area $y \geq 0$ and Darcy’s law is applied for porous medium. A transverse uniform magnetic force field $B_0$ is inflicted across the $y$-axis. The geometry of the considered flow phenomena is depicted in Figure 1. The governing equations for the fluid flow model are formulated as [24,30,31]

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0, \quad (1)$$

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = \nu \left( \frac{\partial^2 u}{\partial y^2} + \frac{3(n-1)}{2} \Gamma_2 \frac{\partial^2 u}{\partial y^2} \left( \frac{\partial u}{\partial y} \right)^2 \right) - u \left( \frac{\sigma B_0^2}{\rho} + \frac{v}{K_1} \right), \quad (2)$$

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \frac{1}{\rho c_p} \left( \frac{\partial}{\partial y} \left( k(T) \frac{\partial T}{\partial y} \right) \right) + D_T \frac{\partial^2 T}{\partial y^2}, \quad (3)$$

$$u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} = D_{SM} \frac{\partial^2 C}{\partial y^2} + D_{CT} \frac{\partial^2 T}{\partial y^2}. \quad (4)$$
The corresponding conditions on the boundaries are as follows

\[
\begin{align*}
    u &= u_w = ax, \quad v = v_w, \quad T = T_w, \quad C = C_w \text{ at } y = 0, \\
    u &\rightarrow 0, \quad T \rightarrow T_\infty, \quad C \rightarrow C_\infty \text{ as } y \rightarrow \infty. 
\end{align*}
\]  
(5)

In the above model, (1) is the continuity equation, (2) is the momentum equation, (3) is the energy equation, and (4) is the concentration equation. The terms \( u, v \) represent components of velocity along \( x \) and \( y \) directions respectively, \( \rho, \sigma, \) and \( \nu \) represents density, electrical conductivity, and the kinematic viscosity of the considered fluid respectively, \( D_{CT} \) is Soret type diffusivity, \( D_{SM} \) is diffusivity of porous medium, \( D_{TC} \) is Dufour type diffusivity, and \( B_0 \) denotes the applied magnetic force field while \( c_p \) is specific heat and \( K_1 \) is porous medium permeability. Moreover, \( u_w \) is stretching velocity of the sheet, \( v_w \) is mass transfer velocity, \( T, T_w, \) and \( T_\infty \) represent, respectively, the fluid temperature, temperature of the wall, and the ambient temperature, \( C, C_w, \) and \( C_\infty \) are, respectively, the concentration, concentration at the wall, and free stream concentration, \( \Gamma \) is the material time constant, \( n \) is the power law index describing fluid characteristics, while \( k(T) = k^* \left( 1 + \beta \frac{T - T_\infty}{T_w - T_\infty} \right) \) is the variable thermal conductivity.

The following similarity transformations are considered to transform the governing equations

\[
\begin{align*}
    \eta &= \sqrt{a \nu} y, \quad \psi = \sqrt{a \nu x} f(\eta), \\
    \theta &= \frac{T - T_\infty}{T_w - T_\infty}, \quad \phi = \frac{C - C_\infty}{C_w - C_\infty}. 
\end{align*}
\]  
(6)

Subject to these similarity transformations, Equation (1) is automatically satisfied whereas Equations (2)–(4) with the boundary conditions (5) are transformed to the dimensionless form as

\[
\begin{align*}
    f''' - (f')^2 + ff'' + \frac{3(n-1)}{2} W e^2 (f'')^2 f''' - (M^2 + \lambda) f' &= 0, \\
    \theta'' + \beta(\theta\theta'' + (\theta')^2) + Pr f\theta' + P_r N_\delta \phi'' &= 0, \\
\end{align*}
\]  
(7, 8)
\[ \phi'' + Le(f\phi') + L_d\theta'' = 0, \quad (9) \]
\[ f'(\eta) = 1, f(\eta) = S, \theta(\eta) = 1, \phi(\eta) = 1 \text{ at } \eta = 0, \]
\[ f'(\eta) \to 0, \theta(\eta) \to 0, \phi(\eta) \to 0 \text{ as } \eta \to \infty. \quad (10) \]

Equations (7)–(9) are the transformed equations subject to the boundary conditions (10). In these equations, \( n \) is called the power law index, \( We^2 = \frac{\nu^2 \beta^2}{\rho} \) represents Weissenberg number, \( \lambda = \frac{\nu}{\rho} \) is porosity parameter, \( M^2 = \frac{\nu^2 \beta^2}{\rho} \) is Hartmann number, \( Pr = \frac{\nu}{\rho} \) and \( N_d = \frac{D_{rec}(C_0-C_{\infty})}{\nu(T_w-T_{\infty})} \) represent the Prandtl number and modified Dufour parameter, respectively. \( \nu \) is the Lewis number, \( L_d = \frac{D_{rec}(T_w-T_{\infty})}{D_{SM}(C_w-C_{\infty})} \) is the Dufour solutal Lewis number, \( S = \frac{\nu}{\sqrt{\nu}} \) where \( S > 0 \) is for suction while \( S < 0 \) corresponds to injection parameter.

The physical quantities such as skin friction, the Nusselt number and Sherwood number are compared in Table 1.

| Values of \( M \) | Khan et al. [30] | Current Results |
|------------------|----------------|----------------|
| 0                | 1              | 1              |
| 0.5              | -1.1181        | -1.1181        |
| 1                | -1.4141        | -1.4142        |
Figure 2a–d shows the changes in the dimensionless velocity profile $f'(\eta)$ with reference to $M$, the Hartmann number, $We$, the Weissenberg number, $\lambda$, the porosity parameter, and $n$, the power-law index. In Figure 2a, we can see that raising values for $M$ causes a reduction in velocity for both cases of suction and injection. As $M$ corresponds to Lorentz force due to which for larger values of $M$ the Lorentz force enhances and as this force is a resistive force acting against the motion of the fluid hence reduces the fluid’s velocity. Figure 2b illustrates the increasing behavior of the velocity field for $We$ and for $n > 1$. The velocity profile decelerates with larger porosity parameter ($\lambda$) as demonstrated in Figure 2c. This is because $\lambda$ creates more resistance in the fluid due to Darcian drag. Additionally, the changes in velocity are greater in the case of injection as compared to the suction case. The effect of $n$ is displayed in Figure 2d. It is evidently clear from this figure that the velocity enhances when $n$ is increasing. This is because the non-linearity of the sheet is increased with the power-law index which reduces the resistant force and also the non-Newtonian behavior of the fluid is decreased.

Variations in temperature profile ($\theta(\eta)$) of the fluid flow for various parameters are shown in Figure 3. In Figure 3a $\theta(\eta)$ is plotted against the variable thermal conductivity ($\beta$) and shows that temperature increases with higher thermal conductivity. This behavior is observed because the higher the thermal conductivity the higher will be the kinetic energy of the fluid particles which then elevates the temperature. Figure 3b demonstrates the effect of $\lambda$ on $\theta(\eta)$. It is observed that $\theta(\eta)$ is enhancing due to the increase of the porosity parameter $\lambda$. It can also be seen that in the case of injection, the porosity parameter $\lambda$ causes more changes in the temperature. The effects of Prandtl number ($Pr$) on the temperature

Figure 2. Variations in $f'(\eta)$ against $M$ (a), $We$ (b), $\lambda$ (c), and $n$ (d).
field is plotted in Figure 3c. The reason for this particular behavior is that the Prandtl number has an inverse relation with the thermal diffusivity of the fluid so a higher $Pr$ number means low thermal diffusion which then further means a lower temperature is observed. Figure 3d shows the impact of the modified Dufour parameter ($Nd$) on $\theta(\eta)$. It is clear that temperature increases with increasing $Nd$. In Figure 3e,f, the temperature profile against $M$ and power-law index ($n$) are illustrated. It is deduced that $\theta(\eta)$ enhances with increasing $M$ and reduces with $n$. Due to the greater magnitude of the Lorentz force depicted by higher $M$, the resistive force between the layers of the fluid results in an increase in the temperature.

![Graphs showing temperature profiles](image)

Figure 3. Variations in temperature profile against $\beta$ (a), $\lambda$ (b), $Pr$ (c), $Nd$ (d), $M$ (e), and $n$ (f).

In Figure 4a–d the dimensionless concentration profile is plotted against the Hartmann number ($M$), Dufour solutal Lewis number ($Ld$), Lewis number ($Le$), and porosity parameter ($\lambda$). From Figure 4a–d, it is clear that concentration profile ($\phi(\eta)$) and the boundary
layer thickness increases with increasing $M$, $Ld$, and $\lambda$ while decreases with $Le$. The ratio of thermal diffusivity to the mass diffusivity is known as Lewis number due to which at high Lewis number thermal diffusion dominates, and that is why the concentration profile reduces. Due to porosity parameter $\lambda$, mass diffusivity is greater because of which $\phi(\eta)$ increases and $\lambda$ has more effect on concentration in injection than in the suction case.

Figure 4. Variations in concentration profile against $M$ (a), $Ld$ (b), $Le$ (c), and $\lambda$ (d).

Figure 5a,b demonstrates behavior of the skin friction drag against variant values for $M$, $n$ and $\lambda$. From Figure 5a, it is deduced that friction increases with increasing Hartmann number ($M$) and $\lambda$. An increase in $M$ produces more friction between layers and also with the surface of the sheet. The opposite impact of the power-law index ($n$) on the skin friction coefficient is observed in Figure 5b.

The behavior of the local Nusselt number versus different parameters is observed in Figure 6a,b. Figure 6a shows that Nusselt number is decreasing for the variable thermal conductivity ($\beta$) plotted against porosity parameter ($\lambda$). As thermal conductivity increases the transfer of heat through conduction increases which results in a decrease in the Nusselt number. The behavior for the various values of the $Pr$ versus $Nd$ can be seen in Figure 6b. Increasing values of $Pr$ means that momentum diffusivity dominates which results in more heat transfer and so the Nusselt number enhances.

Figure 7a demonstrates the impact of the Dufour solutal Lewis number ($Ld$) against $\lambda$ on the Sherwood number. The results show that the Sherwood number lessens with both $Ld$ and $\lambda$. The effect of the Lewis number ($Le$) versus the modified Dufour parameter ($Nd$) on the local Sherwood number is observed in Figure 7b where it is seen that the Sherwood number elevates with increasing values of $Le$ and $Nd$. 
4. Conclusions

In this article we studied a double-diffusive Carreau non-Newtonian fluid flow with variable thermal conductivity in a porous media. Similarity transformations are used to transform the governing Carreau fluid flow model equations into a system of non-linear ordinary differential equations. Physical quantities of primary interest are investigated for
key parameters present in the study and a skin friction coefficient comparison has been carried out with the results available in [30] for various values of the Hartmann number which show agreement with each other. The impacts of various physical parameters are presented graphically. The following results are obtained from the present study.

- The velocity profile decelerates for increasing Hartmann number ($M$) and porosity parameter ($\lambda$) while increases for Weissenberg number ($We$) and power-law index ($n$).
- The temperature field increases with variable thermal conductivity ($\beta$), $\lambda$, $M$, and with the modified Dufour parameter ($Nd$) while decreases for the Prandtl number ($Pr$) and $n$.
- The concentration profile reduces with the Lewis number ($Le$) while enhances with $M$, the Dufour solutal Lewis number $Ld$, and for $\lambda$.
- The local skin friction drag increases with $M$ and $\lambda$ while reduces with $n$.
- The Nusselt number diminishes with $\beta$, $\lambda$, and $Nd$ while increases with $Pr$.
- The Sherwood number decreases with $Ld$ and $\lambda$ while increases with $Le$ and $Nd$.
- The presence of the suction parameter provides more resistance to the fluid flow as compared to injection.
- The temperature and concentration of a fluid increase in the case of injection parameter.

Author Contributions: Data curation, S.Z.; Formal analysis, M.I.; Investigation, S.A.; Methodology, T.S. All authors have read and agreed to the published version of the manuscript.

Funding: This research received no external funding.

Conflicts of Interest: The authors declare no conflict of interest.

Nomenclature

The following abbreviations are used in this manuscript:

- $T_\infty$: ambient temperature (K)
- $x, y$: Cartesian coordinates
- $C_w$: concentration at the wall (mol/m$^3$)
- $f'$: dimensionless velocity
- $\rho$: density (kg/m$^3$)
- $\mu$: dynamic viscosity (kg/m s)
- $\theta$: dimensionless temperature
- $\phi$: dimensionless concentration
- $D_{TC}$: Dufour type diffusivity (m$^2$/s)
- $Ld$: Dufour solutal Lewis number
- $\sigma$: electrical conductivity (S/m)
- $k^*$: free stream conductivity
- $C_\infty$: free stream concentration (mol/m$^3$)
- $M$: Hartmann number
- $n$: kinematic viscosity (m$^2$/s)
- $Le$: Lewis number
- $B_0$: magnetic field strength (T)
- $v_w$: mass transfer velocity
- $\Gamma$: relaxation time (s)
- $Nd$: modified Dufour parameter
- $Nu_\infty$: Nusselt number
- $Pr$: Prandtl number
- $D_{SM}$: porous medium diffusivity (m$^2$/s)
- $K_1$: porous medium permeability (m$^2$)
- $\lambda$: porosity parameter
- $Re$: Reynolds number
- $a$: stretching rate (s$^{-1}$)
- $\eta$: similarity variable
References

1. Sahoo, B. Flow and heat transfer of a non-Newtonian fluid past a stretching sheet with partial slip. Commun. Nonlinear Sci. 2010, 15, 602–615. [CrossRef]

2. Akbar, N.S.; Nadeem, S.; Haq, R.U.; Khan, Z.H. Numerical solutions of magnetohydrodynamic boundary layer flow of tangent hyperbolic fluid towards a stretching sheet. Indian J. Phys. 2013, 87, 1121–1124. [CrossRef]

3. Hamid, M.; Usman, M.; Khan, Z.H.; Ahmad, R.; Wang, W. Dual solutions and stability analysis of flow and heat transfer of Casson fluid over a stretching sheet. Phys. Lett. A 2019, 383, 2400–2408. [CrossRef]

4. Sharma, R.; Bisht, A. MHD flow of Sisko nanofluid over a stretching sheet with Joule heating. AIP Conf. Proc. 2019, 2134, 030002.

5. Salahuddin, T.; Malik, M.Y.; Hussain, A.; Bilal, S.; Awais, M. MHD flow of Cattaneo–Christov heat flux model for Williamson fluid over a stretching sheet with variable thickness: Using numerical approach. J. Magn. Magn. Mater. 2016, 401, 991–997. [CrossRef]

6. Ullah, Z.; Zaman, G.; Ishak, A. Magnetohydrodynamic tangent hyperbolic fluid flow past a stretching sheet. Chin. J. Phys. 2020, 66, 258–268. [CrossRef]

7. Wang, C.Y. Flow due to a stretching boundary with partial slip—An exact solution of the Navier–Stokes equations. Chem. Eng. Sci. 2002, 57, 3745–3747. [CrossRef]

8. Zaimi, K.; Ishak, A. Stagnation-point flow towards a stretching vertical sheet with slip effects. Mathematics 2016, 4, 27. [CrossRef]

9. Ullah, Z.; Zaman, G. Lie group analysis of magnetohydrodynamic tangent hyperbolic fluid flow towards a stretching sheet with slip conditions. Heligyon 2017, 3, e00443. [CrossRef]

10. Shankaralingappa, B.M.; Madhukesh, J.K.; Sarris, I.E.; Gireesha, B.J.; Prasannakumara, B.C. Influence of thermophoretic particle deposition on the 3D flow of sodium alginate-based Casson nanofluid over a stretching sheet. Micromachines 2021, 12, 1474. [CrossRef]

11. Sowmya, G.; Sarris, I.E.; Vishalakshi, C.S.; Kumar, R.S.V.; Prasannakumara, B.C. Analysis of transient thermal distribution in a convective–radiative moving rod using two-dimensional differential transform method with multivariate Pade approximant. Symmetry 2021, 13, 1793. [CrossRef]

12. Sarada, K.; Gowda, R.J.; Sarris, I.E.; Kumar, R.N.; Prasannakumara, B.C. Effect of magnetohydrodynamics on heat transfer behaviour of a non-Newtonian fluid flow over a stretching sheet under local thermal non-equilibrium condition. Fluids 2021, 6, 264. [CrossRef]

13. Malik, R.; Khan, M.; Shafiq, A.; Mushtaq, M.; Hussain, M. An analysis of Cattaneo-Christov double-diffusion model for Sisko fluid flow with velocity slip. Results Phys. 2017, 7, 1232–1237. [CrossRef]

14. Waqas, M.; Khan, W.A.; Asghar, Z. An improved double diffusion analysis of non-Newtonian chemically reactive fluid in frames of variables properties. Int. Commun. Heat Mass Transf. 2020, 115, 104524. [CrossRef]

15. Haq, R.U.; Nadeem, S.; Khan, Z.H.; Akbar, N.S. Thermal radiation and slip effects on MHD stagnation point flow of nanofluid over a stretching sheet. Phys. E Low Dimens. Syst. Nanostruct. 2015, 65, 17–23. [CrossRef]

16. Shankaralingappa, B.M.; Prasannakumara, B.C.; Gireesha, B.J.; Sarris, I.E. The Impact of Cattaneo–Christov double diffusion on Oldroyd-B fluid flow over a stretching sheet with thermophoretic particle deposition and relaxation chemical reaction. Inventions 2021, 6, 95. [CrossRef]

17. Naveen Kumar, R.; Punith, Gowda, R.J.; Prasanna, G.D.; Prasannakumara, B.C.; Nisar, K.S.; Jamshed, W. Comprehensive study of thermophoretic diffusion deposition velocity effect on heat and mass transfer of ferromagnetic fluid flow along a stretching cylinder. Proc. Inst. Mech. Eng. E J. Process Mech. Eng. 2021, 235, 1479–1489. [CrossRef]

18. Khan, Z.H.; Khan, W.A.; Pop, I. Triple diffusive free convection along a horizontal plate in porous media saturated by a nanofluid with convective boundary condition. Int. Commun. Heat Mass Transf. 2013, 66, 603–612. [CrossRef]

19. Krishna, M.V.; Reddy, G.S. MHD forced convective flow of non-Newtonian fluid through stumpy permeable porous medium. Mater. Today Proc. 2018, 5, 175–183. [CrossRef]

20. Hayat, T.; Qasim, M.; Mesloub, S. MHD flow and heat transfer over permeable stretching sheet with slip conditions. Int. J. Numer. Methods Fluids 2011, 66, 963–975. [CrossRef]
21. Siavashi, M.; Rostami, A. Two-phase simulation of non-Newtonian nanofluid natural convection in a circular annulus partially or completely filled with porous media. *Int. J. Mech. Sci.* 2017, 133, 689–703. [CrossRef]

22. Eldabe, N.T.M.; Sallam, S.N.; Abou-zeid, M.Y. Numerical study of viscous dissipation effect on free convection heat and mass transfer of MHD non-Newtonian fluid flow through a porous medium. *J. Egypt. Math. Soc.* 2012, 20, 139–151. [CrossRef]

23. Khan, M.; Malik, M.Y.; Salahuddin, T.; Khan, I. Heat transfer squeezing flow of Carreau fluid over a sensor surface with variable thermal conductivity: A numerical study. *Results Phys.* 2016, 6, 940–945. [CrossRef]

24. Reddy, G.R.; Naramgari, S. Heat and mass transfer in radiative MHD Carreau fluid with cross diffusion. *Ain Shams Eng. J.* 2018, 9, 1189–1204.

25. Sulochana, C.; Ashwinkumar, G.P.; Sandeep, N. Transpiration effect on stagnation-point flow of a Carreau nanofluid in the presence of thermophoresis and Brownian motion. *Alex. Eng. J.* 2016, 55, 1151–1157. [CrossRef]

26. Khan, M.; Malik, M.Y.; Salahuddin, T. Heat generation and solar radiation effects on Carreau nanofluid over a stretching sheet with variable thickness: Using coefficients improved by Cash and Carp. *Results Phys.* 2017, 7, 2512–2519. [CrossRef]

27. Raju, C.S.K.; Sandeep, N. Falkner-Skan flow of a magnetic-Carreau fluid past a wedge in the presence of cross diffusion effects. *Eur. Phys. J. Plus* 2016, 131, 267. [CrossRef]

28. Amanulla, C.H.; Wakif, A.; Boulahia, Z.; Reddy, M.R.; Nagendra, N. Numerical investigations on magnetic field modeling for Carreau non-Newtonian fluid flow past an isothermal sphere. *J. Braz. Soc. Mech. Sci. Eng.* 2018, 40, 462. [CrossRef]

29. Akbar, N.S.; Nadeem, S.; Khan, Z.H. Numerical simulation of peristaltic flow of a Carreau nanofluid in an asymmetric channel. *Alex. Eng. J.* 2014, 53, 191–197. [CrossRef]

30. Khan, M.; Malik, M.Y.; Salahuddin, T.; Khan, I. Numerical modeling of Carreau fluid due to variable thicked surface. *Results Phys.* 2017, 7, 2384–2390. [CrossRef]

31. Gireesha, B.J.; Archana, M.; Prasannakumara, B.C.; Gorla, R.S.R.; Makinde, O.D. MHD three dimensional double diffusive flow of Casson nanofluid with buoyancy forces and nonlinear thermal radiation over a stretching surface. *Int. J. Numer. Methods Heat Fluid Flow* 2017, 27, 2858–2878. [CrossRef]