Design development and performance evaluation of photovoltaic/thermal (PV/T) hybrid solar dryer for drying of ber (Zizyphus mauritiana) fruit

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Surendra Poonia1*, A.K. Singh1 and Dilip Jain1

Abstract: This research paper describes the drying kinetics of ber (Zizyphus mauritiana) fruit and economic evaluation of hybrid photovoltaic/thermal (PV/T) solar dryer fabricated using locally available materials, e.g. galvanized iron sheet, glass, PV panel and fan. Ber fruits were dried to the safe level moisture content (20%) in a period of 240 h with the drying load of 18 kg. Four mathematical models were evaluated to predict the behaviour of ber (Zizyphus mauritiana) drying in a combined hybrid PV/T solar dryer. Experimental data of moisture ratio (MR) and temperature obtained from dryer were fitted to the four empirical drying models. The performance of the drying model was compared based on their statistical parameters: coefficient of determination ($R^2$), root mean square error (RMSE) and reduced chi-square ($\chi^2$) between the observed and predicted MR. The logarithmic model was found to be the most suitable for describing the thin layer drying behaviour of ber (Zizyphus mauritiana). The effective moisture diffusivity was $3.34 \times 10^{-7}$ m$^2$/s and the efficiency of this dryer was found to be 16.7%. The developed hybrid PV/T drying system produces better quality products in shorter time by the efficient use of solar energy. The economic evaluation of the hybrid photovoltaic thermal (PV/T) solar dryer revealed that high value of IRR (54.5%) and
low value of payback period (2.26 Years) make the dryer unit cost-efficient ensuring its economic viability.

Subjects: Heat Transfer; Heating Ventilation & Air Conditioning; Power & Energy; Design
Keywords: ber drying; PV/T hybrid solar dryer; mathematical modelling; economic evaluation

1. Introduction
Ber or Indian jujube (Ziziphus mauritiana) is generally consumed fresh and is an important fruit of arid regions of India. Jujubes play an important role in human nutrition as sources of sugar, vitamins, protein and minerals (Yi, Wu, Zhang, Li, & Luo, 2012). Short shelf-life and post-harvest rotting are the most important problems in ber fruits. There has been limited post-harvest research on ber fruit in the past two to three decades, and the information is scattered in diverse local and regional sources, especially in India (Pareek & Yahia, 2013). Drying is practised to enhance the storage life, to minimize losses during storage and to reduce transportation costs of agricultural products (Leon, Kumar, & Bhattacharya, 2002). In India, 70% people depend on agricultural practices and of this most farmers are subsistence farmers, and affording hi-tech facilities and equipment is a major problem. Direct sun drying method has been practised since ancient times, and it is still being widely used in developing countries. Although this method of drying is cheap, yet it is associated with the problems like contamination as well as uneven drying.

To overcome these disadvantages, the drying process can be replaced with solar drying or industrial drying methods such as hot air. Mechanical drying which is mainly used in industrialized countries as an alternative to sun drying is not applicable to small farms in India. This is due to its high investment and operating costs. Fortunately, India is blessed with abundant solar energy (Pande et al., 2009). During winter from November to February, most of the Indian stations receive 4.0 to 6.3 kWhm\(^{-2}\) day\(^{-1}\) solar irradiance, while in summer season, this value ranges from 5.0 to 7.4 kWhm\(^{-2}\) day\(^{-1}\). The arid and semi-arid parts of the country receive much more radiation as compared to the rest of the country with 6.0–7.4 kWhm\(^{-2}\) day\(^{-1}\) mean annual daily solar radiation having 8.9 average sunshine hours a day at Jodhpur, India (Pande et al., 2009). Solar drying has been identified as a promising alternative to sun drying for drying of fruit and vegetables in developing countries like India because of its minimal operational cost in terms of fuel cost (Poonia, Singh, Santra, & Jain, 2017; Purohit, Kumar, & Kandpal, 2006). Utilization of solar energy for drying is advantageous because it is a free, low cost, renewable and abundant-energy source besides having environment-friendly and economically viable attributes making it acceptable for use by rural farmers (Sharma, Chen, & Vu Lan, 2009). It is also a more convenient alternative for rural sector and other areas with scarce or irregular electricity supply. Studies conducted on solar drying have proved it to be a good alternative for sun drying for the production of high-quality dried products (Ekechukwu & Norton, 1999; Hossain, Woods, & Bala, 2005; Mahapatra & Imre, 1990; Sodha & Chandra, 1994).

The research and development work for PV/T applications have increased in recent years to conserve the conventional energy sources. Headley (1997) provides the overview of renewable energy systems/technologies (e.g. solar crop drying, PV applications etc.) in the Caribbean (Headley, 1997). Huang, Lin, Hung, and Sun (2001) reported that an integrated PV/T system is economically feasible. Tonui and Tripanagnostopoulos (2007) suggested some low-cost modifications to improve the performance of air-cooled PV/T solar collectors. Tiwari and Sodha (2006a) developed a thermal model of an integrated PV/T solar (IPV/TS) system and reported that the simulations predict a daily thermal efficiency of around 58%, which is very close to the experimental value (61.3%) obtained by Huang et al. (2001). Barnwal and Tiwari (2008) conducted experimental studies of grape drying using hybrid PV/T green house dryer. Very recently Tiwari, Tiwari, and Al-Helal (2016) have developed mathematical model of PV/T mixed mode greenhouse solar dryer. Modelling of the drying process is a valuable tool for prediction of performance of solar drying systems (Sacilik, Keskin, & Elicin, 2006). The thin layer drying model has been found to be most suitable for
characterizing the drying parameters. Several researches on the mathematical modelling and experimental studies had been conducted on the thin layer drying processes of various agricultural products (Arslan and Özcan, 2010; Aghbashlo, Kianmehr, Khani, & Ghasemi, 2009; Corzo, Bracho, Pereira, & Vasquez, 2008; Doymaz, 2005; Doymaz & İsmail, 2011; Goyal, Kingsly, Manikantan, & Ilyas, 2007; Kouchakzadeh & Shafeei, 2010; Zielinska & Markowski, 2010). However, there is little information about thin layer solar drying process of ber fruit in the literature.

The present solar dryer is unique as it uses both thermal and solar photovoltaic simultaneously. The same unit is being used as solar collector as well as solar dryer. The solar photovoltaic fan regulates the temperature uniformly when solar radiation and ambient temperature are high, then the speed of fan is increased. With this in view, a solar dryer having a hybrid PV/T system has been designed and developed at the ICAR-Central Arid Zone Research Institute, Jodhpur, India for ber drying. In this paper, an attempt has been made to evaluate the drying characteristics of ber fruit by fitting four mathematical models for describing the thin-layer drying process for the solar drying of ber. The economic analyses of a hybrid PV/T dryer have also been carried out to study the real-time possibilities for its use in drying process.

2. Materials and methods

2.1. Design of solar dryer

A PV/T hybrid solar dryer was designed and fabricated at the workshop of ICAR-Central Arid Zone Research Institute, Jodhpur, India. The hybrid system has been designed and fabricated in such a way that it enabled the combined production of electrical energy and thermal energy from the photovoltaic panel and flat plate collector, respectively. The drying methodology and steps of drying process are represented according to the flow diagram given in Figures 1(a) and (b). The dryer consists of a collector unit, drying chamber, DC fan, PV panel and PCM chamber for thermal storage. The PV module was provided at left side of solar collector to operate a DC fan for forced mode of operation. Dryer having a size 1250 mm × 850 mm was made by galvanized steel sheet (22 gauge), which consists of four drying trays. The clear window glass (4mm thick) is provided at the top of the box. The area of collector designed for the dryer is 1.06 m² with a DC fan of 10 W, which was used for exhausting moisture with the help of a solar panel of 20 Wp (Figure 2). The dimension of two drying trays made of stainless steel angle frame and stainless steel wire mesh was (0.84 × 0.60 m) and that of two half trays (0.40 × 0.60 m). The drying material can be kept on four trays and placed on angle iron frame in the dryer through an openable door provided on the rear side of the dryer. Six plastic pipes are fixed in the back wall of the dryer just below the trays to introduce fresh air at the base. Actual installation of the PV/T hybrid solar dryer is shown in Figure 3.
2.2. Experimental procedure

Ber (Zizyphus mauritiana) fruit used for the drying experiment was procured from a local market, and the selection was based on visual assessment of uniform colour and geometry. The drying trial for dehydrating ber (Zizyphus mauritiana) in this dryer was conducted in the month of January, 2017. During the drying process, the moisture loss of samples was determined by means of a
digital electronic balance (Testing Instrument Pvt Ltd., India) having an accuracy of ± 0.001 g. The PVT hybrid dryer was loaded with 18 kg of fresh ber fruits having 80% moisture content on wet basis. Hourly total solar insolation received on the horizontal plane was measured by pyranometer coupled with integrator. Air temperature inside the dryer and ambient temperature were measured hourly from 08:00 h to 18:00 h during the drying trials. Moisture content of the ber fruits during each day was computed from difference in these weighs.

The initial moisture content of the ber on wet basis was determined using the relation according to AOAC (AOAC, 2000).

\[
Mi = \left( \frac{Wi - Wf}{Wi} \right) \times 100
\]  

(1)

where \(M_i\) is the initial moisture content of ber on wet basis expressed in %, \(W_i\) is the initial weight of ber in g and \(W_f\) is the final weight of ber in g. The recorded moisture contents for each sample were then used to plot the drying curves. The drying rate (DR) of ber fruits was calculated using following equation.

\[
DR = \frac{\Delta M}{\Delta t}
\]  

(2)

where

\(\Delta M = \text{loss of the mass of the crop (kg water/kg dry matter) and } \Delta t = \text{interval of time (min)}\).

2.3. Mathematical modelling of drying curves and formulation

The moisture ratio (MR) and the drying rate (DR) of ber (Zizyphus mauritiana) fruit were calculated using the following equations during the drying experiments:

\[
MR = \frac{M_t - M_e}{M_0 - M_e}
\]  

(3)

\[
DR = \frac{M_t + dt - M_t}{dt}
\]  

(4)

where \(M, M_0, M_e, M_t\), and \(M_{t+dt}\) are the moisture contents at a given time, initial moisture content, equilibrium moisture content, moisture content at the time of \(t\) and moisture content at the time of \(t+dt\) (kg water/kg dry matter), respectively. However, MR is simplified to \(M_t/M_0\) because \(M_e\) is very small.
compared with $M_t$ and $M_0$ (Jain and Pathare, 2007; Midilli and Kucuk, 2003; Yaldiz, Ertekin, & Ibrahim Uzun, 2001).

Mathematical models that describe drying mechanisms of fruit and vegetables provide the required temperature and moisture information (Doymaz, 2012; Goyal et al., 2007; Koukouch et al., 2015). Thin-layer drying models can be categorized as theoretical, semi-theoretical and empirical models. Some semi-theoretical drying models that have been widely used in the literature (Henderson and Pabis (1961) model, the Lewis model (Bruce, 1985), the Page model (Page, 1949) and logarithmic model (Doymaz, 2007) were tested. These models are generally derived by simplifying general series solution of Fick’s second law. These models were fitted in the experimental data in their linearized form using regression technique. The selected models used to explain the drying data of ber are described below.

2.3.1. The Henderson and Pabis model
The Henderson and Pabis model is the first term of a general series solution of Fick’s second law. Bi-parametric exponential model is another definition of this model. The Henderson and Pabis model has produced good correlations in predicting the drying of corn (Henderson & Pabis, 1961) and pumpkins (Hashim, Daniel, & Rahaman, 2014). This model can be written as:

$$\frac{M - M_e}{M_0 - M_e} = a \exp (-kt)$$  \hspace{1cm} (5)

where $a$ and $k$ are the constants of the model and $t$ is the drying time.

2.3.2. The Lewis model (newton model)
The Lewis model is a special case of the Henderson and Pabis model where intercept is unity. It was used to describe drying characteristics of barley (Bruce, 1985) and strawberry (El-Beltagy, Gamea, & Amer Essa, 2007). The model is given in the following form:

$$\frac{M - M_e}{M_0 - M_e} = \exp (-kt)$$  \hspace{1cm} (6)

where $k$ is the constants of the model and $t$ is the drying time.

2.3.3. The page model
The Page model is an empirical modification of the Lewis model that corrects some shortcomings. This model has been used to describe the drying of many agricultural products, such as corn (Page, 1949), pistachio nuts (Kashaninejad, Mortazavi, Safekordi, & Tabil, 2007), long green pepper (Akpinar & Bicer, 2008) and green soybean (Yang & Zhu, 2015). This model is given as:

$$\frac{M - M_e}{M_0 - M_e} = \exp(-kt^n)$$  \hspace{1cm} (7)

where $k$ and $n$ are the constants of the model and $t$ is the drying time.

2.3.4. Logarithmic model
The Henderson and Pabis model was modified by adding an empirical constant ($c$) to get the logarithmic model. It was successfully used to describe the drying characteristics of apricots (Toğrul & Pehlivan, 2002) and pumpkin slices (Doymaz, 2007). This model is expressed as:

$$\frac{M - M_e}{M_0 - M_e} = a \exp (-kt) + c$$  \hspace{1cm} (8)

where $a$, $k$ and $c$ are the constants of the model and $t$ is the drying time.

2.4. Data analysis
The drying rate constants and coefficients of all of the models were estimated using the non-linear least square regression analysis, which was performed using SPSS (Statistical Package for Social
Scientists) 11.5.1 software package. The coefficient of determination ($R^2$) is one of the main criteria for selecting the best simulation equation of the drying curve best-fitting sample. The other factors are the chi-square value ($\chi^2$) and the root mean square value (RMSE). A high degree of fitting equations should have the highest coefficient of determination ($R^2$), lower chi-square value ($\chi^2$) and root mean square error (RMSE) (Gbaha, Yobouet Andoh, Kouassi Saraka, Kamenan Koua, & Toure, 2007; Madhlopa, Jones, & Kalenga, 2002; Roberts, Singh, & Cunba, 2000; Tunde-Akintunde, Afolabi, & Akintunde, 2005). These statistical parameters were calculated according to the following equations:

$$R^2 = 1 - \frac{\sum_{i=1}^{N} (MR_{exp,i} - MR_{pre,i})^2}{\sum_{i=1}^{N} (MR_{pre,i})^2}$$  \hspace{1cm} (9)$$

$$\chi^2 = \frac{\sum_{i=1}^{N} (MR_{exp,i} - MR_{pre,i})^2}{N - z}$$  \hspace{1cm} (10)$$

$$RMSE = \sqrt{\frac{\sum_{i=1}^{N} (MR_{exp,i} - MR_{pre,i})^2}{N}}$$  \hspace{1cm} (11)$$

where $MR_{exp,i}$ and $MR_{pre,i}$ are experimental and predicted MRs, respectively; $N$ is number of observations; and $z$ is number of drying constants.

### 2.5. Estimation of effective moisture diffusion coefficient

Effective moisture diffusion coefficient ($D_{eff}$) reflects dehydration ability of materials under certain drying conditions and is a significant transport property in modelling the drying process of biological materials, as a function of temperature and moisture content in materials (Doymaz, 2012). The simplified mathematical Fick's second law for diffusion was used to estimate the effective diffusion coefficient of the ber fruit during drying. Analytical solution of Fick's second law is given in the Eq.(12), considering a constant moisture diffusivity, infinite slab geometry and uniform initial moisture distribution (Doymaz, 2012).

$$MR = \frac{M - M_e}{M_0 - M_e} \sum_{n=1}^{\infty} \frac{1}{n^2} \exp \left( -\frac{n^2 \pi^2 D_{eff} t}{4r^2} \right)$$  \hspace{1cm} (12)$$

where $D_{eff}$ is the effective diffusivity coefficient (m$^2$/s), $r$ is the half thickness of the samples (m), $n$ is the positive integer and $t$ is the drying time (s). For long drying times (setting $n = 1$), Saravacos and Raouzeos (1986) demonstrated that Eq. (12) could be further simplified to a straight-line equation and can be expressed in a logarithmic form by taking the natural logarithm of both sides.

$$\ln (MR) = \ln \left( \frac{8}{\pi^2} \right) - \left( \frac{\pi^2 D_{eff} t}{4r^2} \right)$$  \hspace{1cm} (13)$$

The effective moisture diffusivity was calculated using the method of slopes. It is typically determined by plotting experimental drying data in terms of $\ln(MR)$ versus time (Doymaz, 2006). From Eq. (13), a plot of linear regression of $\ln(MR)$ versus drying time gives a straight line with a slope of:

$$\text{slope} = \left( \frac{\pi^2 D_{eff}}{4r^2} \right)$$  \hspace{1cm} (14)$$

Then the effective moisture diffusion coefficient ($D_{eff}$) was calculated according to the slope, which was obtained by the linear fitting.
2.6. Thermal efficiency ($\eta$)

The efficiency of utilization of solar energy in solar dryer (ratio of heat used in evaporation of moisture from ber to the incident total solar radiation on horizontal plane) has been worked out using the following relation (Leon et al., 2002; Poonia et al., 2017):

$$\eta = \frac{ML}{A \int_{0}^{\theta} H \, d\theta} \quad (15)$$

where $A$ = Absorber area ($m^2$); $H$ = Solar radiation on horizontal plane ($J \, m^{-2} \, hr^{-1}$); $L$ = Latent heat of vaporization ($J \, kg^{-1}$); $M$ = Mass of moisture evaporated from the product ($kg$); $\theta$ = Period of test (hr) and $\eta$ = Efficiency of the solar dryer.

3. Results and discussion

3.1. Drying characteristics

The maximum stagnation temperature observed inside the drying chamber was $70^\circ C$ and on loading 18 kg of ber, the maximum temperature reduced to $64^\circ C$, when the outside ambient temperature was $23^\circ C$. The variation of solar insolation, ambient temperature and temperature inside upper and lower tray of dryer, when ber fruit was loaded during the drying trails, is shown in Figure 4. It can be seen that the effect of drying temperature on the required drying time was considerably pronounced, which is in agreement with the results from several food materials, such as plums (Goyal et al., 2007), pumpkin slices (Doymaz, 2007), pistachio nuts (Kashaninejad et al., 2007) and castor oil seeds (Perea-Flores et al., 2012).

The variation of measured moisture content (wet basis) of the ber fruits on each day of drying trials was shown in Figure 5. It can be seen that the moisture content was reduced from about 80% to 26% within 8 days by the solar drying method and on tenth day it came to 20%. However, after 8 days (26% moisture content), it could be safely stored for further use when the moisture content falls below 66%, the drying rate in the solar dryer increases sharply. The shape of the drying curve indicates a rapid moisture removal from the product at the initial stage, which later decreased with increase in drying time. Thus, the MR decreased continually with drying time. This continuous decrease in MR indicates that diffusion has governed the internal mass transfer. This is in agreement with the results of study on figs (Piga, Pinna, Ozer, Agabbio, & Aksoy, 2004), lettuce and cauliflower leaves (Lopez, Iguaz, Esnoz, & Virsed, 2000) and ber (Das & Dutta, 2013), tomatoes (Doymaz, 2007) and amasya red apples (Doymaz, 2010).
3.2. Fitting of drying models

The four drying models (Henderson and Pabis model—Eq. (5); Lewis model—Eq. (6); Page model—Eq. (7); and that of Logarithmic model—Eq. (8)) were used to fit the drying data obtained to estimate the MR as a function of drying time. The statistical analyses undertaken on the drying data to evaluate the models for experimental condition (i.e. parameters such as coefficient of determination ($R^2$), chi-square ($\chi^2$) and root mean square error (RMSE) obtained using Eqs. (9–11) are shown in Table 1. The model that best predicts the drying process will have higher values of $R^2$, and lower values of $\chi^2$ and RMSE. For all the models, the ranges of $R^2$, $\chi^2$ and RMSE values were between 0.9881 and 0.9982, 0.000047 and 0.00014 and 0.007338 and 0.012605, respectively. Overall, it could be revealed that the logarithmic model presented the higher $R^2$ values, whereas their $\chi^2$ and RMSE values were relatively lower than those for the other tested models (Table 1). The higher values of $R^2$ for logarithmic model show that it represents a better correlation between the MR and drying time than the other models. Therefore, according to the results from Table 1, logarithmic model was best-suited compared with other models, and this model was chosen as the optimal model providing satisfactory descriptions of drying characteristics of ber fruits. The values of $R^2$ obtained from all the models were higher than the acceptable $R^2$ value of 0.97 (Shen et al., 2011).

The experimental and predicted MR by the logarithmic model for ber fruit was shown in Figure 6. It can be observed from the figure that the experimental MR was, in general, in line with the predicted ones. It is clearly indicated that this model could be used to describe the MR variation during the drying process. The logarithmic model was also reported by other researchers as the most suitable model to explain the drying behaviour and MR evolution of apricot (Faal, Tavakoli, & Ghobadian, 2015); black grapes (Domyaz, 2006); chilli pepper (Tunde-Akintunde, 2011); onion slices (Sharma, Verma, & Pathare, 2005) and water chestnut (Singh, Sharma, Bawa, & Saxena, 2008).

![Figure 5. Variation of moisture content in ber solar drying against drying time.](image)

| Model name       | $R^2$   | $\chi^2$  | RMSE   |
|------------------|---------|-----------|--------|
| Henderson and Pabis | 0.9900  | 0.00014   | 0.012586 |
| Lewis model      | 0.9881  | 0.00041   | 0.012605 |
| Page             | 0.9913  | 0.000013  | 0.012188 |
| Logarithmic      | 0.9982  | 0.000047  | 0.007388 |
3.3. Effective moisture diffusivity ($\text{d}_{\text{eff}}$)

The effective moisture diffusivity computed using the graph of ln (MR) against time was shown in Figure 7. It can be observed that the $D_{\text{eff}}$ of ber fruits was $3.34 \times 10^{-7}$ m$^2$/s during the experiment for a loading rate of 18 kg. The value of the effective moisture diffusion coefficients obtained from the experiment was similar to the results by some researchers, from $7.20 \times 10^{-9}$ to $1.91 \times 10^{-8}$ m$^2$/s for the thin-layer drying of sweet sorghum stalks at 30–70°C (Shen et al., 2011) and $4.08 \times 10^{-8}$ to $2.35 \times 10^{-7}$ m$^2$/s for convective drying of pumpkin at 30–70°C (Hashim et al., 2014). According to reports (Wang et al., 2007), the values of effective diffusivity fall within the range of $10^{-11}$ to $10^{-7}$ m$^2$/s for all agricultural and food products.

3.4. Dryer overall efficiency

The overall efficiency of the drying is affected by several factors such as drying time, climatic conditions (solar insolation and temperature), the drying characteristics of the dried materials and structure of the drying devices etc. The average efficiency of utilization of solar energy in the solar dryer was calculated by Eq. (15), and it was found that about 16.7% solar energy was utilized in this solar dryer. During drying process, it was observed that higher efficiency was observed at initial stage of drying, later stage this dryer efficiency decreased due to decrease in moisture content. Moreover, the efficiency was more at a higher drying load of 18 kg which might be due to highest drying time.
4. Economic analysis of PV/T hybrid solar dryer
The PV/T hybrid solar dryer was used for drying ber (Zizyphus mauritiana) fruits. The economic analysis of the present dryer was carried out by computing the life cycle cost (LCC) and life cycle benefit (LCB) of the dryer. In addition, five economic attributes, namely, benefit-cost ratio (BCR), net present worth (NPW), annuity (A), internal rate of return (IRR) and pay-back period (PBP), were also determined for judging the economic viability of the dryer (Table 3).

4.1. Life cycle cost (LCC)
LCC of the PV/T hybrid solar dryer is the sum of all the costs associated with a solar drying system over its lifetime in terms of money value at the present instant of time and it takes into account the time value of money (Kalogirou, 1996). The initial investment (P) of the dryer unit is INR 14,000. The annual cost of operation and maintenance (O&M) including labour are taken as INR 4000. The salvage value is taken as 10% of initial investment.

4.1.1. Determination of (LCC)
Economics of PV/T hybrid solar dryer was calculated through LCC analysis. Let \( P_i \) be the initial investment (INR), \( P_w \) the operational and maintenance expenses including replacement costs for damaged components (INR), \( n \) the life of the dryer (Year), \( P_w \) (SV) the salvage value of the dryer at the end of the dryer’s life (INR). The procedure of LCC estimation as adopted by Barnwal & Tiwari, 2008; Sohda, Chandra, Pathak, Singh, & Bansal, 1991 is given as,

\[
LCC \text{ (Unit)} = P_i + P_w \times \frac{X(1-X^n)}{1-X} - SV \times (1 + i)^{-n}
\]

\[
= 14000 + 4000 \times \frac{X(1-X^n)}{1-X} - 1400 \times (1 + i)^{-n}
\]

\[
= 14000 + 4000 \times \frac{X(1-10^{0.04})}{1-1} - 1400 \times (1 + 0.1)^{-10}
\]

where \( X = \frac{1+e}{1+i} \), \( e = \) annual escalation in cost (in fraction) and \( i = \) interest or discount rate (in fraction).

| Sr. No. | Attributes economics | Values |
|---------|----------------------|--------|
| 1       | BCR                  | 1.86   |
| 2       | NPW                  | 37018  |
| 3       | A                    | 4989   |
| 4       | IRR (per cent)       | 54.50  |
| 5       | PBP (years)          | 2.26 years |

Table 3. Values of economic attributes

Table 2. Values of NPW for different rates of discount/interest (i)

| NPW (INR) | 37,018.59 | 981.98 | -3,376.83 |
|-----------|-----------|--------|----------|
| Interest rate \( i \) (%) | 10 | 50 | 70 |
4.2. Life cycle benefits (LCB)

The values of $R$ (annual benefit) are obtained using the dryer for 10 trials each for ber ($Zizyphus mauritiana$) and seed less lasoda/gonda. The quantity of ber to be dried was about 180 kg costing about 3,600 Indian Rupees. The dried ber was about 60 kg, which fetched (accrued) about INR 9,000/- at a rate of 150 INR/kg. The ensuring benefit of INR 5,400/-. Similarly 10 trials of seedless lasoda/gonda dried about 180 kg gonad, which ensured INR 30/kg benefit on raw seedless gonda amount to about INR 5,400/-. Thus, the total annual benefit from dried product was about INR 10,800/-.  

The LCB can be given as,

$$LCB = R \frac{(1 - X^n)}{(1 - X)}$$  \hspace{1cm} (17)$$

where $R$ = annual benefit (INR) and $X = \frac{1+i}{1+i}$.

4.3. Economic attributes

(i) **BCR**: The ratio of discounted benefits to the discounted values of all costs given as LCB/LCC.

(ii) **NPW**: It is the sum of all discounted net benefits throughout the project given as LCB-LCC.

(iii) The annuity (A) of the project indicates the average net annual returns given as,

$$(\text{Annuity}) = \frac{NPW}{\sum_{t=1}^{10} \left( \frac{1+i}{1+i} \right)^n}$$

(iv) **PBP**: It is the length of time from the beginning of the project before the net benefits return the cost of capital investments (value $n$ for LCB—LCC = 0).

(v) **IRR**: It is that rate of interest which makes LCB and LCC equal (LCB—LCC = 0)

4.3.1. Determination of economic attributes

(i) **BCR**: The ratio of discounted benefits to the discounted values of all costs can be expressed as:

$$\text{Benefit cost ratio (BCR)} = \frac{\text{Life cycle benefits of hybrid solar dryer}}{\text{Life cycle cost of hybrid solar dryer}}$$

$$BCR = \frac{R \frac{(1 - X^n)}{(1 - X)}}{P_i + P_w - P_w (SV)} = \frac{LCB}{LCC} = \frac{80171}{43153} = 1.86$$

(ii) $\text{NPW} = \text{LCB} - \text{LCC} = 37018$

(iii) The annuity (A) of the project indicates the average net annual returns. This term can be given as,

$$A(\text{Annuity}) = \frac{NPW}{\sum_{t=1}^{10} \left( \frac{1+i}{1+i} \right)^n} = \frac{37018}{7.42} = 4989$$

(iv) Pay-back period can be determined as following: $-\text{LCC} + \text{LCB} = 0$

Or $14000 + 4000 x$

$$\frac{0.945 (1 - 0.945^n)}{(1 - 0.945)} = 10800 \frac{0.945 (1 - 0.945^n)}{(1 - 0.945)}$$

Or $14000 = 6800 \frac{0.945 (1 - 0.945^n)}{(1 - 0.945)}$
Or \( (1 - 0.945^n) = \frac{14000 (0.055)}{6800 \times 0.945} \)

Or \( 0.945^n = 1 - \frac{14000 (0.055)}{6800 \times 0.945} = 0.8802 \)

Or \( \log 0.945 = \log 0.8802 \)

\[ n = \frac{\log (0.8802)}{\log (0.945)} \]

\[ n = 2.26 \text{ year} \]

Or Pay-back period (PBP) = 2.26 year

(v) **Internal rate of return (IRR):**

The values of NPW at varying discount rates are given in Table 2. From Table 2, it is evident that at 10% interest rate the NPW is INR37,018.59/- and at 50% rate of interest the NPW is INR981.98. However, the NPW is negative at 70% interest rate (i.e. NPW = INR –3376.83/-). The IRR can be determined using data presented in Table 2 and the following relationship:

\[ IRR = \text{lower discount rate} + \frac{\text{Difference of discount rate} \times \text{NPW at lower discount rate}}{\text{NPW at lower discount rate} - \text{NPW at higher discount rate}} \]

\[ IRR = 50 + \frac{20 \times 981.98}{981.98 + 3376.83} = 54.5\% \]

The IRR which comes to 54.5% in the present case, is very high for a project to be economically viable.

The values of five economic attributes, namely, BCR, NPW, A, IRR and PBP are presented in Table 3.

5. **Conclusion**

The drying characteristics of the ber (Zizyphus mauritiana) fruit using a (PV/T) hybrid solar dryer were studied by fitting the data to four models, namely, Henderson and Pabis, Newton, Logarithmic and Page. The drying process involves accelerating rate and falling rate periods, and no constant rate drying period was observed. Three statistical tools were used to quantify the goodness of fitting: the determination of coefficient \( R^2 \), the reduced chi-square \( \chi^2 \) and root mean square error (RMSE). The logarithmic model, which gave higher values of coefficient of determination and lower values of reduced chi-square and RMSE, was considered as the best for predicting the drying characteristics of solar dried ber fruit. The economic parameters such as, IRR and PBP (2.26 years) make the unit very cost-effective. This solar dryer reduced the moisture content from 80% to 20% within 240 h. The use of this hybrid PV/T dryer will prove to be a boon for remote location/rural area with less reliable conventional energy sources. It will go a long way in reducing post-harvest losses as well as CO\(_2\) emission.

**Nomenclature**

- \( A \) absorber area \((m^2)\)
- \( a \) drying constant
- \( b \) drying constant
- \( D_{e\text{ff}} \) effective diffusivity \((m^2 \text{ s}^{-1})\)
- \( H_T \) solar radiation on horizontal plane \((J \text{ m}^{-2} \text{ hr}^{-1})\)
\[ \begin{align*}
  k & \quad \text{drying constant, (l/min)} \\
  L & \quad \text{latent heat of vaporization (J kg}^{-1}) \\
  M & \quad \text{mass of moisture evaporated from the product (kg)} \\
  M_e & \quad \text{equilibrium moisture content, (kg water/kg dry matter)} \\
  M_o & \quad \text{initial moisture content, (kg water/kg dry matter)} \\
  MR & \quad \text{moisture ratio (dimensionless)} \\
  MR_{exp} & \quad \text{experimental moisture ratio} \\
  MR_{pre} & \quad \text{predicted moisture ratio} \\
  M_t & \quad \text{moisture content, (kg water/kg dry matter)} \\
  n & \quad \text{drying constant, positive integer} \\
  N & \quad \text{number of observations} \\
  R & \quad \text{ideal gas constant, (kJ/mol K)} \\
  r & \quad \text{the half-thickness of the samples (m)} \\
  R^2 & \quad \text{coefficient of determination} \\
  RMSE & \quad \text{root mean square error} \\
  W_i & \quad \text{initial weight of product (g)} \\
  W_f & \quad \text{final weight of product (g)} \\
  \chi^2 & \quad \text{reduced chi-square} \\
  t & \quad \text{drying time, min} \\
  T & \quad \text{temperature, (°C)} \\
  z & \quad \text{number of constants in models} \\
  \eta & \quad \text{efficiency of the solar dryer.} \\
  \theta & \quad \text{period of test (hr)}
\end{align*} \]

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