Where are the Fermi Lines Coming From?

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We estimate the spatial locations of sources of the observed features in the Fermi-LAT photon spectrum at \(E_\gamma = 110\) and \(E_\gamma = 130\) GeV. We determine whether they are consistent with emission from a single source, as would be expected in their interpretation as \(\gamma\gamma\) and \(\gamma Z\) lines from dark matter annihilation, as well as whether they are consistent with a dark matter halo positioned at the center of the galaxy. We take advantage of the per-photon measured incident angle in reconstructing the line features. In addition, we use a data-driven background model rather than making the assumption of a feature-less background. We localize the sources of the features at 110 and 130 GeV. Assuming an Einasto (NFW) density model we find the 130 GeV line to be offset from the galactic center by 285 (280) pc, the 110 GeV line by 60 (30) pc with a large relative separation of 220 (240) pc. However, we find this displacement of each source from the galactic center, as well as their relative displacement to be statistically consistent with a single Einasto or NFW dark matter halo at the center of the galaxy.

PACS numbers:

INTRODUCTION

The search for the particle nature of dark matter is one of the outstanding open questions of modern physics. A broad program of research with a variety of promising and complementary approaches has become a major piece of experimental particle physics research. This includes searches for direct production at colliders, searches for dark matter interactions with standard model particles in large quiet underground detectors, and searches for signals of dark matter annihilation into standard model particles in regions of the galaxy with large dark matter density.

A clear signal of dark matter annihilation may be carried by gamma rays traveling to Earth from regions in the galaxy with high dark-matter density. As the photons do not typically scatter after their production, the photon energy and direction are powerful handles for understanding the mechanism of dark matter annihilation into standard model particles.

One mechanism is annihilation resulting in quarks, which would hadronize and yield \(\pi^0\) particles which in turn produce photons. The broad spectrum of such a process would give fairly low energy photons (\(E_\gamma \lesssim 50\) GeV) and may be difficult to distinguish from other sources.

A clearer signature may appear from annihilation directly into two-body final states including a photon, though the rate would be smaller than continuum emission due to loop suppression. Rather than yielding a broad energy spectrum, this process would produce a photon with a well-defined energy (a “line”). This makes a search for lines in the photon spectrum an important component of the dark matter program using Fermi-LAT data [1-3].

Recently, observation of a feature with high local statistical significance at \(E_\gamma = 130\) GeV was reported [4, 5], with a source location 1-2 degrees away from the galactic center [6]. Follow-up analyses suggested the possibility of two features, consistent with the spacing of lines expected from \(\gamma\gamma\) and \(\gamma Z\) processes [7, 8].

In this paper, we study in detail the question of the location of the source of the photons in the features. We confirm the location of the photons in the feature at \(E_\gamma = 130\) GeV, and for the first time, locate the source of the photons in the feature at \(E_\gamma = 110\) GeV. We study whether the two are – individually or collectively – consistent with emission from a single source, as would be expected if they represent the \(\gamma\gamma\) and \(\gamma Z\) processes, as well as whether that source is consistent with a dark matter halo at the galactic center. In addition, we introduce a new approach to analyzing the data which uses the measured angles of the individual photons, rather than the median photon angles.

ENERGY SPECTRUM ANALYSIS

A source of photons with a very narrow range of energies would appear in the spectrum of observed Fermi-LAT photons as a peak, due to finite energy resolution. Previous analyses [4, 7, 8] have used the Fermi-LAT energy dispersion formula [9] to build a probability density function (pdf) for the reconstructed energies of photons from a line, and fit it to the observed spectrum.

Given the small size of the dataset, we seek to use the maximum available information about each photon to extract insight into the observed features. The energy resolution, for example, has a significant dependence on two other photon characteristics: \(\theta\), the incident angle relative to a line normal to the LAT face, and the photon “type” which indicates whether the conversion happened in the front or back layers of the tracker [10]. Figure [1]...
shows the reconstructed energy pdf for various choices of \( \theta \) and type. This per-photon information is very pertinent to the analysis of this spectrum. If the photons in the peak were all well-measured, it would enhance the significance of the peak; conversely, if they were all poorly-measured, it would degrade the significance.

Our approach is to reconstruct the distribution of \( E_{\gamma}^{\text{true}} \), the true energy of photons striking the LAT, rather than the distribution of \( E_{\gamma}^{\text{reco}} \), the reconstructed energy of each photon. The former distribution can account for the per-photon resolution, while the latter treats each photon equally. The reconstructed energy is related to the true energy by the pdf \( f(E_{\gamma}^{\text{reco}}|E_{\gamma}^{\text{true}}, \theta, \text{type}) \). We use Bayes theorem to invert this relation and calculate \( E_{\gamma}^{\text{true}} \). The distribution of photons in the peak region and the background region have similar median photon angles. As the distribution of photons in photon angles has peaks at 110 and 130 GeV which are formation. The spectrum which uses the measured per-photon information, but it remains a useful method to visualize this demonstrates the range of possibilities, if all photons had demonstrated the impact of this information. Two choices of priors have negligible effect, as the energy dispersion pdf is sharply peaked, see Fig. 1.

The distribution of \( E_{\gamma}^{\text{true}} \) is then built as a kernel density estimate \([11]\) with \( f(E_{\gamma}^{\text{true}}|E_{\gamma}^{\text{reco}}, \theta, \text{type}) \) as the choice of kernel. Other approaches \([5, 6]\) have used adaptive Gaussian kernels, but our physically motivated choice of kernel reflects the asymmetric shape of the pdf and uses – for the first time – the per-photon measured incident angle rather than the median angle of the dataset.

We use the publicly available Fermi-LAT data collected over 3.7 years. We use ultraclean photons with zenith angle < 100 to veto photons from Earth as well as standard quality requirements \([12]\). We select a three-degree region around the galactic center.

The observed photon counts in the three-degree region are shown in Fig. 2. The distribution of \( E_{\gamma}^{\text{true}} \) is shown in Fig. 3 with several choices of angle-dependence used to demonstrate the impact of this information. Two choices demonstrates the range of possibilities, if all photons had the maximum or minimum possible energy resolutions. This demonstrates the potential importance of this information. The spectrum which uses the measured per-photon angles has peaks at 110 and 130 GeV which are slightly degraded relative to a spectrum which uses the median photon angle. As the distribution of photons in the peak region and the background region have similar distributions of \( \cos(\theta) \) and conversion type \([13]\), there is not currently a large impact from using the per-photon information, but it remains a useful method to visualize the spectrum.

**LOCATING THE FEATURES**

**Technique**

We search for the most likely source position using a maximal likelihood fit of the observed photons to the expected spatial and energy distributions from dark matter halos. The unbinned likelihood is

\[
L(l, b) = \frac{\prod_i n_{\text{bg}} f_{\text{bg}}(E_i, \theta_i) + n_{\text{sig}} f_{\text{sig}}(E_i, l, b_i | \theta_i, l, b)}{n_{\text{bg}} + n_{\text{sig}}}
\]

where \( (l, b) \) are the galactic coordinates of the center of the dark matter halo, \( n_{\text{bg}} = n_{\text{sig}} \) are the background and signal normalizations, the index \( i \) runs over observed photon energy and spatial parameters \( (E_i, \theta_i, l_i, b_i) \) within the energy window surrounding the
features of interest, and \( f_{\text{sig}}(E_{\gamma}, l, b | \theta, l, b) \) is the dark matter halo pdf as a function of photon energy \( E_{\gamma} \), incidence angle \( \theta \), at spatial position \((l, b)\) given a dark matter halo centered at \((l, b)\). The pdf \( f_{\text{sig}} \) accounts for per-photon spatial \([14]\) and energy \([9]\) resolution in the same spirit as the Bayesian unfolding described above; here we do not need to explicitly unfold, as we have included the per-photon information in the unbinned likelihood.

The background pdf \( f_{\text{bg}} \) is built from a data-driven model, with the energy dependence coming from photons outside the three-degree region surrounding the galactic center, see Figure 4. We find this to be reasonably consistent with a power law model used in previous analyses \([4–8]\). We use energy windows of \( E_{\gamma} = [105, 115], [125, 135] \) for the location of the feature at 110 GeV and 130 GeV, respectively, or both windows for the combined features. In the case of the two-feature analysis \( (E_{\gamma} = 110, 130 \text{ GeV}) \), there are two \( f_{\text{sig}} \) terms in the likelihood, one for each peak. We use normalizations of \( n_{\text{sig}} = 6 \) and \( n_{\text{sig}} = 14 \) for the \( E_{\gamma} = 110 \) and 130 GeV features, respectively.

The dark matter halo pdfs \( f_{\text{sig}} \) are derived from either NFW \([15]\) or Einasto \([16]\) halo profiles; the pdf in \((l, b)\) is calculated via the line-integral of the square of the dark matter density \([17]\). We use \( \alpha_E = 0.17 \) for the Einasto model and \( r_s = 20 \text{ kpc} \) for both models.

Results

The position of the most likely values of the halo centers are given in Table 1 for both DM profiles and each of the features as well as the combined spectrum. In both cases, the feature at 130 GeV appears to be displaced from the galactic center, as previously reported, but the

![FIG. 3: Relative likelihood of true photon energies, \( E_{\gamma}^{\text{true}} \), built from the reconstructed energies of Fig 2 and the pdf \( f(E_{\gamma}^{\text{true}} | E_{\gamma}^{\text{ reco}}, \theta, \text{type}) \), see text for details. The impact of different assumptions about the photon incident angle \( \theta \) is shown.](image)

![FIG. 4: The data-driven background model (points) constructed from photons outside the three-degree region surrounding the galactic center, compared to a power law with exponent -2.6.](image)

110 GeV feature appears to be centered at the galactic origin.

![FIG. 5: Most likely positions in galactic coordinates \((l, b)\) of an NFW (top) or Einasto (bottom) dark matter halo, maximized separately for the features at 130 GeV, 110 GeV, or the combined features. Also shown are 1\( \sigma \) and 2\( \sigma \) uncertainty regions, see text for details.](image)
TABLE I: Most likely positions in galactic coordinates \((l, b)\) of an NFW or Einasto dark matter halo, maximized separately for the features at 130 GeV, 110 GeV, or the combined features.

| E\(_\gamma\) \[GeV\] | True \(E\gamma\) \[GeV\] | Background subtracted weight |
|----------------------|----------------------|-----------------------------|
| \(80\)               | \(90\)               | \(0\)                        |
| \(100\)              | \(110\)              | \(0.5\)                      |
| \(120\)              | \(130\)              | \(1\)                        |
| \(140\)              | \(150\)              | \(1.5\)                      |
| \(160\)              | \(170\)              | \(2\)                        |
| \(180\)              | \(140\)              | \(2.5\)                      |

If the observed features are both due to dark matter annihilation processes, then their locations in the sky depend only on the dark matter density and not the nature of the final state, \(\gamma \gamma\) or \(\gamma Z\), and so should yield locations consistent with a single source. As shown above, we find that the sources of the \(E\gamma = 110\) and 130 GeV features are separated appreciably from each other, and that the \(E\gamma = 130\) feature is displaced from the galactic center.

Definitive conclusions, however, require analysis of the uncertainties involved, including the expected fluctuations of the measured source locations given the small number of photons in each feature. We seek to answer two questions:

- Are the two features consistent with emission from a single source?
- Are the features consistent with emission from a dark matter halo at the galactic center?

We answer these questions by comparing hypotheses using likelihood ratios. For example, we can probe whether the feature at \(E\gamma = 130\) GeV is consistent with emission from the galactic center by evaluating

\[
q = -2 \log \left( \frac{L(l = \hat{l}, b = \hat{b})}{L(l = 0, b = 0)} \right)
\]

where \((\hat{l}, \hat{b})\) is the location which maximizes \(L\) and \((0, 0)\) serves as the null hypothesis. When \((\hat{l}, \hat{b})\) is close to \((0, 0)\), the log of the likelihood ratio \(q\) approaches zero; when it is far from the origin, it becomes negative. We compare the measured value of \(q\) to the expected distribution in simulated experiments from an NFW or Einasto profile with a line at \(E\gamma = 130\) GeV placed at \((0, 0)\), see Figures 8(a) and 9(a). While the value of \(q\) indicates that the maximal position is displaced from the origin, it is consistent with the expected distribution of \(q\) values when the DM halo is at the origin; the \(p\)-values = 0.18 and 0.14 for Einasto or NFW, respectively. Distributions of \(q\) for DM halos offset from the origin are also shown.

We perform this analysis for the feature at \(E\gamma = 110\) GeV as well, see Figures 8(b) and 9(b). As this feature appears to be located close to \((0, 0)\), the \(q\) values are close to zero and entirely consistent with a DM halo at the galactic center.

We repeat the analysis for the combined features at 110 and 130 GeV, where we constrain them to have the same location, see Figures 8(c) and 9(c). Again, the \(q\) values are consistent with a DM halo at the galactic center.

To address the question of whether the two features are more likely to be from a single source (consistent with a DM interpretation) or from two spatially distinct sources, we construct a likelihood ratio...
\[
q = -2 \log \frac{L_{130}(\hat{l}, \hat{b}) \times L_{110}(\hat{l}, \hat{b})}{L_{130}(\hat{l}_{130}, \hat{b}_{130}) \times L_{110}(\hat{l}_{110}, \hat{b}_{110})}
\]  

where in one case we find the single location \((\hat{l}, \hat{b})\) which maximizes \(L\) for both features, and in the other we allow the two features to find individual maxima: \((\hat{l}_{110}, \hat{b}_{110})\) and \((\hat{l}_{130}, \hat{b}_{130})\). This \(q\) will be zero if the individually optimized (and possibly separated) locations are consistent with the most likely single joint location, and positive if individually optimized (and possibly separated) locations give a better description of the data. Again we compare to the expected distribution of the likelihood ratio in simulated experiments in which the two sources are co-located and find that the observed \(q\) is consistent with a co-located source, see Figures 8(d) and 9(d).

FIG. 8: The log of likelihood ratios comparing the likelihood of an Einasto DM halo placed at the most likely position \((\hat{l}, \hat{b})\) or at the galactic center \((l = 0, b = 0)\), in the case of the 130 GeV feature (a), the 110 GeV feature (b), or the combined features (c). Also shown is the likelihood ratio between two co-located sources or sources which are separated (d). In each case, we show the expected distribution in simulated experiments.

Different from the standard approach of assuming the median angle and therefore resolution.

We have presented an analysis of the spatial locations of the sources of the observed features in the Fermi-LAT energy spectrum at \(E_{\gamma} = 110\) and 130 GeV. We find:

- the 130 GeV photons come from a location displaced from the galactic center, but consistent with an Einasto or NFW dark matter halo at the center. This is consistent with previous work [17].
- the 110 GeV photons come from a location close to the galactic center, and consistent with an Einasto or NFW dark matter halo at the center.
- the two features at 110 and 130 GeV photons are consistent with a single DM halo at the galactic center, with either an Einasto or NFW density profile.

Some have suggested that the displacement of the source of the \(E_{\gamma} = 130\) GeV feature indicates that DM halos may be displaced from the galactic center [18], but we find that the current data are consistent with a DM halo from the center.

CONCLUSION

We have demonstrated via Bayesian unfolding the potential importance of including the per-photon energy resolution, though for this dataset the results are little

FIG. 9: The log of likelihood ratios comparing the likelihood of an NFW DM halo placed at the most likely position \((\hat{l}, \hat{b})\) or at the galactic center \((l = 0, b = 0)\), in the case of the 130 GeV feature (a), the 110 GeV feature (b), or the combined features (c). Also shown is the likelihood ratio between two co-located sources or sources which are separated (d). In each case, we show the expected distribution in simulated experiments.
ACKNOWLEDGEMENTS

The authors acknowledges contributions, explanations and useful discussions with Eric Albin which are clearly deserving of authorship, clever statistical insight from Kyle Cranmer, useful comments from Annika Peter, and technical support from Mariangela Lisanti and Tracy Slatyer. DW and KR are supported by grants from the Department of Energy Office of Science and by the Alfred P. Sloan Foundation. DW is grateful to the Aspen Center for Physics, where a portion of this work was performed and supported by NSF grant no. 1066293.

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