Calcite Kinks Grow via a Multistep Mechanism

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ABSTRACT: The classical model of crystal growth assumes that kinks grow via a sequence of independent adsorption events where each solute transitions from the solution directly to the crystal lattice site. Here, we challenge this view by showing that some calcite kinks grow via a multistep mechanism where the solute adsorbs to an intermediate site and only transitions to the lattice site upon the adsorption of a second solute. We compute the free energy curves for Ca and CO$_3$ ions adsorbing to a large selection of kink types, and we identify kinks terminated both by Ca ions and by CO$_3$ ions that grow in this multistep way.

1. INTRODUCTION

Calcite, a common biomineral and the most abundant carbonate on Earth, has been the subject of extensive experimental and computational study. However, our understanding of the molecular mechanisms underpinning calcite growth remains limited. While ion adsorption to calcite steps has been comprehensively studied using molecular simulation, studies of kinks have been limited to only a few kink types or focused on energy calculations on non-aqueous calcite. Calcite kink growth is a complex process involving the attachment and detachment of ions to and from 16 unique kink sites. A more comprehensive study is therefore required to gain insights into the molecular processes that constitute calcite kink growth.

Crystal growth models usually treat the attachment of units to kinks as independent elementary events, whereas the kinks are structured such that the terminating ion occupies its lattice site upon adsorption. The structure of kink sites has consequences for the study of the interactions between impurities and kinks. The role of impurities in crystallization has been the focus of various experimental studies, ranging from their retardation of crystal growth to their morphological and mechanical impact. Molecular simulation is able to complement such studies through determining binding configurations and calculating binding free energies. However, such studies assume that the terminating ions of kinks occupy their lattice site. Computational studies of kink nucleation have already revealed a more complex picture where lone CO$_3$ ions are found to prefer to reside above the step, rather than adsorbing directly to the lattice sites. A similar complex process has been observed for barite. Because kinks do not nucleate through the straightforward process of direct adsorption of units onto crystal lattice sites, we cannot assume that they propagate in such a way.

In this study, we determine the free energy curves for Ca and CO$_3$ ions adsorbing to 12 out of 16 kink types, revealing each thermodynamically stable kink configurations. By simulating the dual adsorption of a CO$_3$ ion and a Ca ion to a kink, we show that ions that adsorb preferentially to a bidentate configuration will transition to the lattice site after a second ion adsorbs.

2. METHODOLOGY

The free energy surfaces for Ca and CO$_3$ ions adsorbing to a selection of calcite kinks were computed using metadynamics. Calcite has 16 unique kinks on each side of its glide plane: four kink geometries, labeled (a–d) in Figure 1, each of which can be terminated by either Ca(i), CO$_3$(i), Ca(ii), or CO$_3$(ii), where (i) and (ii) represent the alternating carbonate orientations along each step. The free energy surfaces were computed for a Ca ion adsorbing to each of the eight CO$_3$-terminated kinks; a CO$_3$ ion adsorbing to four of the eight Ca-terminated kinks; and the dual adsorption of a CO$_3$ ion and a Ca ion to one type of Ca-terminated kink. For each kink site, the ion that terminates the kink is tethered to the exact position of its bulk lattice site using a radial harmonic potential with a spring constant of 100 kJ/mol/Å. When this was applied...
to CO$_3^-$ only the C atom was constrained in this potential. Additionally, in order to prevent its drift, the calcite slab was held in place by setting the total momentum of the slab (excluding the adsorbate) to zero at every timestep.

Molecular dynamics simulations were performed using LAMMPS. The inter- and intra-molecular interactions for Ca and CO$_3^-$ as well as their interactions with water, were described by the force field of Raiteri et al. which was explicitly fitted to reproduce the experimentally found solubility of calcite. The self-interactions of water were described by SPC/Fw. Periodic boundaries were used in all dimensions, and a monoclinic skew was added to the simulation box in order to accommodate a slab of calcite periodic in the x- and y-directions, including an elevated step and two exposed kink sites. The slab of calcite was separated from its periodic image in the z-direction by a gap filled with water molecules. Free energy surfaces were computed using well-tempered metadynamics as implemented in Plumed.

The reaction coordinates depended on the simulation, as highlighted green and yellow regions correspond to the lattice and bidentate configurations (see Figure 2).

\[ \Delta G_{ads} = -k_B T \log \left( \frac{P_{ads}}{P_{diss}} \right) \]  

(1)

where $P_{ads}$ and $P_{diss}$ are the equilibrium probabilities of finding a solute in an adsorbed and dissolved state, respectively, when the solute is dissolved in solution at a concentration of 1 mol.

As the adsorption free energy has a well-defined meaning and does not depend on any experimental or simulation conditions, it makes an ideal quantity to calculate. $\Delta G_{ads}$ can be computed with an entropic correction to $\Delta G_{sim}$ as detailed in the Supporting Information.

2.1. Ca Adsorption. For a Ca ion adsorbing to a CO$_3^-$-terminated kink, the z coordinate of the Ca ion [its position normal to the (10.4) surface] was chosen as the reaction coordinate. The Ca ion was confined to a region in the (x, y) plane, centered on the target adsorption site using harmonic barriers. Explicitly dehydrating the Ca ion can be important in some reactions, but it had negligible effect on the free energy surfaces in the case of Ca adsorption to kinks (see the Supporting Information).

The average number of water molecules coordinated with the adsorbing Ca ion, $\langle N_i \rangle$, was measured while the ion was in its most stable bound configuration

\[ N_i = \sum_j \chi_j, \quad \chi_j = \begin{cases} 1, & r_j \leq r_0 \\ 0, & r_j > r_0 \end{cases} \]  

(2)

where $r_j$ is the distance to water oxygen $j$ and $r_0 = 3$ Å is a cutoff distance. The value of 3 Å is chosen from radial distribution functions previously computed by Raiteri et al.

2.2. CO$_3^-$ Adsorption. For a CO$_3^-$ ion adsorbing to a Ca-terminated kink, the CO$_3^-$ ion was confined to a region in the (x, y) plane using harmonic barriers, and two reaction coordinates were used: the z coordinate of the CO$_3^-$ ion and, to drive dehydration of the kink, the distance between the kink-terminating Ca ion and its nearest water molecule. More precisely, we used an approximation of this nearest distance
where \( r_j \) is the distance to water oxygen \( j \) and \( \beta \) is a constant. For an appropriately chosen \( \beta \), this function is a continuously differentiable approximation of the smallest \( r_j \), making it suitable as a reaction coordinate (a similar approximation has been used elsewhere\(^7\)). A justification for this reaction coordinate can be found in the Supporting Information.

### 3. RESULTS AND DISCUSSION

#### 3.1. Ca Adsorption Free Energies

We calculated the free energy surfaces for a Ca ion adsorbing to eight different CO\(_3\) terminated kinks as a function of the Ca-kink z-distance (Figure 1). Table 1 summarizes the simulation free energy differences and adsorption free energies (\( \Delta G_{\text{ads}} \)) for Ca and CO\(_3\) ions adsorbing to various kink types. \( \langle N_\beta \rangle \) is the average water coordination number of the Ca adsorbate in its most stable configuration.

| ion  | kink | \( \Delta G_{\text{sim}} \) (kJ/mol) | \( \Delta G_{\text{ads}} \) (kJ/mol) | \( \langle N_\beta \rangle \) |
|------|------|-------------------------------------|-------------------------------------|-----------------------------|
| Ca   | a(i) | 30                                   | 32                                  | 3                           |
|      | a(ii) | 36                                   | 26                                  | 2                           |
|      | b(i)  | 35                                   | 25                                  | 4.6                         |
|      | b(ii) | 31                                   | 20                                  | 3.2                         |
|      | c(i)  | 39                                   | 29                                  | 4.5                         |
|      | c(ii) | 24                                   | 15                                  | 3.1                         |
|      | d(i)  | 42                                   | 31                                  | 2.8                         |
|      | d(ii) | 46                                   | 26                                  | 2.7                         |
| CO\(_3\) | a(i) | 46                                   | 32                                  | -                           |
|       | a(ii) | 49                                   | 36                                  | -                           |
|       | d(i)  | 52                                   | 38                                  | -                           |
|       | d(ii) | 46                                   | 33                                  | -                           |

\(^{*}\)The ion adsorbs preferentially to the bidentate configuration.

Table 1. Simulation Free Energy Differences (\( \Delta G_{\text{sim}} \)) and Adsorption Free Energies (\( \Delta G_{\text{ads}} \)) for Ca and CO\(_3\) Ions Adsorbing to Various Kink Types. \( \langle N_\beta \rangle \) is the average water coordination number of the Ca adsorbate in its most stable configuration.

The \( \Delta G_{\text{sim}} \) values shown in Table 1 vary between \(-14.7\) and \(-30.8\) kJ/mol. The variation of these numbers is unsurprising because similar calculations for step sites show significant variation in binding free energies.\(^1\) Nevertheless, it is clear that different Ca-terminated kink sites have different stabilities. The free energy profiles show that the position of the thermodynamic minimum depends on the kink type; some kinks prefer the lattice configuration while others prefer the bidentate configuration (Figure 2). Ca ions prefer to adsorb to the lattice configuration in 6 of the 8 cases. For \( a \) and \( d \) kink types, all Ca ions have a thermodynamic minimum at the lattice site. For \( b \) and \( c \) kink types, we find a greater variation in the free energy landscapes, where some prefer the bidentate configuration. Where the lattice configuration is preferred, \( \langle N_\beta \rangle \) corresponds to roughly 3, implying that a total of three coordinated water molecules is the most stable configuration (see Table 1). Where the bidentate configuration is preferred, \( \langle N_\beta \rangle \) is typically about 4.5, implying that the number of coordinated water molecules fluctuates between 4 and 5. Snapshots of each Ca kink in its most stable configuration are shown in Figure S5.

#### 3.2. CO\(_3\) Adsorption Free Energies

The free energy surfaces for a CO\(_3\) ion adsorbing to four different Ca-terminated kinks are shown in Figure 1. The complete free energy landscapes are shown in Figure S6. Table 1 summarizes the simulation free energy differences and adsorption free energies. Unlike Ca kinks, of which all eight were studied, we have only shown the results for four kinks. This is because any attempts to study \( b \) or \( c \) CO\(_3\) kinks resulted in a water molecule becoming trapped under the kink-terminating Ca ion during the simulation. In this situation, the Ca ion would otherwise transition to its bidentate configuration. However, due to the harmonic tethering of the Ca ion, it was unable to do so. The result was that the simulation configurations became unstable, and metadynamics simulations ran into convergence issues. This issue could be solved by applying a dual adsorption method such as the one discussed in Section 2.3. However, these simulation require a far longer convergence time (~3 \( \mu s \)) and are therefore beyond the scope of this study.

The free energies show that CO\(_3\) ions generally adsorb more strongly than Ca ions. The adsorption energies for the CO\(_3\) adsorbates also show less spread than for the Ca adsorbates, with a total span of 5 kJ/mol between the lowest and highest values, compared to 16 kJ/mol for Ca. Local free energy minima correspond to both lattice and bidentate configurations. The lattice configuration requires the full dehydration of the Ca-terminated kink site to which the CO\(_3\) ion binds, while the bidentate configuration does not. Significantly, half of the CO\(_3\)-terminated kink sites prefer to adopt the bidentate configuration. Only the CO\(_3\) kinks have a preference for the lattice configuration. By contrast, Ca ions mostly preferred the lattice configuration. This difference is likely explained by the water molecules at Ca-terminated kinks, the residence times of which are likely to be far larger than those of lone Ca ions.\(^{24}\) The removal of water at kink sites therefore comes at a larger free energy cost than the removal of

![Figure 2](https://pubs.acs.org/doi/10.1021/acs.jpcc.2c04116)
water at lone ions. The most stable bound configurations of CO$_3$ ions are shown in Figure S7.

3.3. Example of a Multistep Kink Growth Mechanism. Because Ca and CO$_3$ ions adsorb preferentially to the bidentate configuration for some of the kinks, it cannot be assumed that kinks always grow via the sequential adsorption of ions directly to the lattice sites. Rather, the adsorption of ions into the lattice sites must involve a more complex process, where ions transition to the lattice site only after the adsorption of a second solute (and possibly more). To demonstrate such a mechanism, we calculated the free energy surface for a CO$_3$ ion and a Ca ion adsorbing to a d(i) Ca-terminated kink (Figure 3).

There are four distinct steps to the growth process, labeled A–D in Figure 3. First, the CO$_3$ ion adsorbs to the kink in the bidentate configuration (A). The Ca ion then adsorbs to the bidentate CO$_3$ ion by sitting approximately 5 Å above the step (B). The CO$_3$ ion transitions to the lattice site, pulling the Ca ion into a bidentate configuration (C). This comes at a free energy cost. Finally, the Ca ion transitions into its lattice configuration (D). This completes the process of adsorption, and it is found that D is the most stable configuration. This result is significant as it demonstrates that even the CO$_3$ ion with the least stable lattice configuration is stabilized at the lattice configuration through the insertion of one additional ion. We also note that three of the four kink types studied have a preference for the bidentate configuration, while all a and d Ca kinks prefer to adopt their lattice configuration. We therefore expect a similar multistep process to occur for all other a and d CO$_3$ kink types. It is worth stressing, however, that the mechanism demonstrated here is only an example of a multistep kink growth mechanism, and that we are not assuming that this result will carry over to other kink types which reside in a bidentate configuration. Nevertheless, the results shown in Figure 2 demonstrate that many terminating ions (4 of the 12 studied) must require one (or more) additional ions to adsorb before a full transition to the lattice site can take place. Ideally, all kink types which prefer to sit in their bidentate configuration should be studied. However, the free energy plot shown in Figure 3 took a total of 3 μs to converge. Repeating this process for five kink types would require multiple simulations over very large time-scales and is therefore beyond the scope of this paper.

3.4. Role of Cation Dehydration in Limiting Kink Growth. Cation dehydration is generally believed to limit the rate of ionic crystal growth, although recent evidence suggests this may not be true for the growth of calcium minerals. For adsorption into the bidentate configuration, our simulation results broadly support this new perspective: we find that, for all of the kinks that we have sampled, the ions must overcome only a $\sim 1 k_B T$ barrier to transition from solution to the bidentate configuration. The solutes will therefore initially adsorb to kinks at a rate determined by diffusion rather than by a reaction barrier.

For some kinks, the lattice configuration is more stable than the bidentate configuration, and there typically exists a substantial barrier from the latter to the former. However, because the barrier from bidentate to solution is generally larger than the barrier from bidentate to lattice, the adsorbate is effectively captured by the kink site as soon as it reaches the bidentate configuration.

4. CONCLUSIONS

Many of the ions that terminate calcite kinks have a tendency to reside in a bidentate configuration, rather than fit directly into the lattice. They sit above the kink, binding to two ions and causing minimal displacement of water molecules. The integration of these ions into the kink lattice site requires the adsorption of an additional ion, and so calcite kinks do not generally grow via a sequence of independent adsorption events as assumed in classical models. This multistep kink propagation process is analogous to what is observed for kink growth.
nucleation, in which solutes initially adsorb to the upper
terrace before the adsorption of another ion. Future molecular
simulation studies of impurities adsorbing to kinks must
therefore take into account whether the kink to which an
impurity binds resides in its lattice or bidentate configuration.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at
https://pubs.acs.org/10.1021/acs.jpcc.2c04116.

Simulation parameters and cell dimensions, discussion on
dehydrating Ca adsorbates, discussion on dehydrating
Ca-terminated kinks, discussion on calculating free
energy surfaces, metadynamics parameters, discussion on
calculating adsorption free energies from simulation
free energy differences, derivation of formula relating
simulation free energy differences and adsorption free
energies, schematic of simulation cell detailing cell sizes,
free energy plots for Ca adsorbates with dehydration
included as a collective variable, comparison of Ca
adsorbate free energies with and without dehydration
included as a collective variable, all Ca adsorbate free
energies as a function of their z-distance from the kink
site, snapshots from simulations detailing the most stable
bound state of each Ca adsorbate, free energy for every
CO3 adsorbate as a function of its distance from the kink
site and the hydration of the kink site, and snapshots
from simulations detailing the most stable bound state
for each CO3 adsorbate (PDF)

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Notes

The authors declare no competing financial interest.

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