Extended Hα over compact far-infrared continuum in dusty submillimeter galaxies
Insights into dust distributions and star-formation rates at z ∼ 2

Chian-Chou Chen (陳建州)1,2, C. M. Harrison3,2, I. Smail4, A. M. Swinbank3, O. J. Turner3, J. L. Wardlow6, W. N. Brandt7,8,9, G. Calistro Rivera10,12, S. C. Chapman11,12,13,14, E. A. Cooke4, H. Dannerbauer15,16, J. S. Dunlop5, D. Farrah17,18, M. J. Michalowski19, E. Schinnerer20, J. M. Simpson1, A. P. Thomson21, and P. P. van der Werf10

1 Academia Sinica Institute of Astronomy and Astrophysics, P.O. Box 23-141, Taipei 10617, Taiwan
e-mail: ccchen@asiaa.sinica.edu.tw
2 European Southern Observatory, Karl Schwarzschild Strasse 2, Garching, Germany
3 School of Mathematics, Statistics and Physics, Newcastle University, Newcastle upon Tyne, NE1 7RU, UK
4 Centre for Extragalactic Astronomy, Department of Physics, Durham University, South Road, Durham DH1 3LE, UK
5 Institute for Astronomy, University of Edinburgh, Royal Observatory, Blackford Hill, Edinburgh EH9 3HJ, UK
6 Physics Department, Lancaster University, Lancaster, LA14YB, UK
7 Department of Astronomy & Astrophysics, 525 Davey Lab, The Pennsylvania State University, University Park, PA 16802, USA
8 Institute for Gravitational and the Cosmos, The Pennsylvania State University, University Park, PA 16802, USA
9 Department of Physics, The Pennsylvania State University, University Park, PA 16802, USA
10 Leiden Observatory, Leiden University, P.O. Box 9513, 2300 RA Leiden, the Netherlands
11 Department of Physics & Astronomy, University of Victoria, BC, V8X 4M6, Canada
12 Department of Physics and Atmospheric Science, Dalhousie University, Halifax, NS, B3H 4R2, Canada
13 NRC Herzberg Astronomy and Astrophysics, 5071 West Saanich Road, Victoria, BC, V9E 2E7, Canada
14 Department of Physics and Astronomy, University of British Columbia, Vancouver, BC, V6T 1Z1, Canada
15 Instituto de Astrofísica de Canarias (IAC), E-38205 La Laguna, Tenerife, Spain
16 Universidad de La Laguna, Dpto. Astrofísica, E-38206 La Laguna, Tenerife, Spain
17 Department of Physics and Astronomy, University of Hawaii, 2505 Correa Road, Honolulu, HI 96822, USA
18 Institute for Astronomy, 2680 Woodlawn Drive, University of Hawaii, Honolulu, HI 96822, USA
19 Astronomical Observatory Institute, Faculty of Physics, Adam Mickiewicz University, ul. Słoneczna 36, 60-286 Poznań, Poland
20 Max—Planck Institut für Astronomie, Königstuhl 17, 69117 Heidelberg, Germany
21 The University of Manchester, Oxford Road, Manchester, M139PL, UK

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ABSTRACT

Using data from ALMA and near-infrared (NIR) integral field spectrographs including both SINFONI and KMOS on the VLT, we investigate the two-dimensional distributions of Hα and rest-frame far-infrared (FIR) continuum in six submillimeter galaxies at z ∼ 2. At a similar spatial resolution (∼0.5 FWHM; ∼4.5 kpc at z = 2), we find that the half-light radius of Hα is significantly larger than that of the FIR continuum in half of the sample, and on average Hα is a median factor of 2.0 ± 0.4 larger. Having explored various ways to correct for the attenuation, we find that the attenuation-corrected Hα-based SFRs are systematically lower than the IR-based SFRs by at least a median factor of 3 ± 1, which cannot be explained by the difference in half-light radius alone. In addition, we find that in 40% of cases the total V-band attenuation (A_V) derived from energy balance modeling of the full ultraviolet(UV)-to-FIR spectral energy distributions (SEDs) is significantly higher than that derived from SED modeling using only the UV-to-NIR part of the SEDs, and the discrepancy appears to increase with increasing total infrared luminosity. Finally, considering all our findings along with the studies in the literature, we postulate that the dust distributions in SMGs, and possibly also in less IR luminous z ∼ 2 massive star-forming galaxies, can be decomposed into three main components: the diffuse dust heated by older stellar populations, the more obscured and extended young star-forming Hα regions, and the heavily obscured central regions that have a low filling factor but dominate the infrared luminosity in which the majority of attenuation cannot be probed via UV-to-NIR emissions.

Key words. Galaxies: formation – Galaxies: ISM – Galaxies: high-redshift – Galaxies: structure – Galaxies: star formation – Submillimeter: galaxies

1. Introduction

Measurements of star-formation rate (SFR) across cosmic time provide one of the most fundamental constraints to models of galaxy formation and evolution (e.g., Somerville & Davé 2015). Comparisons between SFR and other galaxy properties have yielded essential insights into the physics of galaxy assembly, such as the Schmidt-Kennicutt relationship (Schmidt 1959; Kennicutt 1989) and the so-called galaxy star-forming main sequence (e.g., Noeske et al. 2007; Elbaz et al. 2011; Whitaker et al. 2012; Schreiber et al. 2015).
The vital role that SFR measurements play in constraining galaxy models means that the calibrations and diagnostics for various tracers have been extensively studied (Kennicutt & Evans 2012). Thanks to technical advances in both ground-based telescopes and space-based satellites, SFRs can be estimated through a wide spectral range of emissions from X-ray to radio, using both continuum and line emission (e.g., Ranalli et al. 2003; Lehmer et al. 2010; Murphy et al. 2011). Since measurements made at different wavelengths are sensitive to different ages of the stellar populations (Calzetti 2013), and they are affected by dust attenuation to a different level, in principle SFR tracers at different wavelengths should all be considered and exploited for their complementary strengths of diagnostics. Indeed in the local universe, calibrations have been derived to obtain the total SFRs, in particular in addressing dust attenuation, by combing UV, Hα, and infrared data (Hao et al. 2011). This has been done both locally for individual star-forming regions (Calzetti et al. 2007; Li et al. 2013) and globally for entire galaxies (Kennicutt et al. 2009; Catalán-Torrecilla et al. 2015; Brown et al. 2017).

Beyond the nearby universe, the volume-averaged SFR density rises rapidly, by over an order of magnitude by $z \sim 2$ (Madau & Dickinson 2014). During these times the SFR density is dominated by infrared bright galaxies (Le Floc’h et al. 2005; Smolčić et al. 2009; Gruppioni et al. 2013; Swinbank et al. 2014), which are classified as (Ultra-)luminous infrared galaxies ((U)LIRGs; Sanders & Mirabel 1996) with total infrared luminosity greater than $(10^{12} - 10^{13}) L_\odot$. This means that at $z \sim 2$ the infrared component of the SFRs becomes dominant, and the correction of dust attenuation becomes critical for galaxy samples in which the SFRs are predominantly measured via UV and optical. Indeed, continuum and emission lines in the UV and optical are extensively used at high redshifts to measure SFRs given their accessibility and technical advances, and the cosmic SFR density has been estimated with this method up to $z \sim 10$ (e.g., Reddy & Steidel 2009; Bouwens et al. 2011; Ellis et al. 2013; Oesch et al. 2015; McLeod et al. 2016; Ishigaki et al. 2018).

However the method to correct for dust attenuation for UV and optical measurements at high redshifts is currently a topic of debate. For example, the common method to correct the UV SFRs using the correlation between the ratio of infrared and UV luminosity and the spectral slope in the UV, the IRX-$\beta$ relation, is subject to many systematics including turbulence, the age of the stellar populations, and the dust compositions and geometry (e.g., Howell et al. 2010; Casey et al. 2014; Chen et al. 2017; Popping et al. 2017; Narayanan et al. 2018). Similarly, due to the faintness of Hα, the correction for the Hα-based SFRs using the Balmer decrement is also not straightforward. To bypass the difficulty of obtaining the Balmer decrement, stellar attenuation derived from SED fitting based on UV-to-NIR photometry has been adopted (e.g., Sobral et al. 2013). However the relation between the nebular attenuation and the stellar attenuation has not been well determined, both locally (e.g., Kreckel et al. 2013) and at high redshifts (e.g., Calzetti et al. 2000; Wild et al. 2011; Kashino et al. 2013; Price et al. 2014; Reddy et al. 2015; Puglisi et al. 2016; Theios et al. 2018).

Regardless of whether the galaxies are located in the nearby universe or at high redshifts, one of the main issues faced when correcting dust attenuation has been the spatial distribution of dust. It is assumed that dust acts as a foreground screen and spatially coincides with the underlying emissions, which is partly motivated by the findings in the local spiral galaxies (e.g., Kennicutt et al. 2009; Bendo et al. 2012). In addition, motivated by often times different attenuations found in nebular emission lines such as Hα compared to the stellar continuum (e.g., Calzetti et al. 2000), the dust distribution is normally perceived as having two main components; the diffuse dust in the interstellar medium (ISM) that obscured older stellar populations and the dustier component obscuring the Hii regions (e.g., Wild et al. 2011; Price et al. 2014; Reddy et al. 2015; Leslie et al. 2018). This two-component dust distribution model is one of the major assumptions that goes into the SED modeling that employs the energy balance technique, such as magphys (da Cunha et al. 2008, 2015) and cigale (Noll et al. 2009).

In more chaotic and gas-rich environments, in particular at $z \sim 2$, there is increasing evidence suggesting that the aforementioned assumptions may need to be adjusted. For example, studies using ALMA have found, almost ubiquitously, that the massive dusty galaxies at high redshifts have very compact morphology in FIR continuum, with half-light radius of $\sim 1 – 2$ kpc (e.g., Simpson et al. 2015; Ikarashi et al. 2015; 2017; Barro et al. 2016; Harrison et al. 2016; Hodge et al. 2016, 2019; SPIkler et al. 2016; Tadaki et al. 2017a; Oteo et al. 2017; Fujimoto et al. 2018). In addition, many other tracers of star-forming regions are found to be spatially offset from, or much larger than, the FIR continuum, including the stellar continuum in UV/optical (e.g., Chen et al. 2015; Hodge et al. 2016; Cowie et al. 2018; Gómez-Guijarro et al. 2018), radio continuum at 1.4 and 3 GHz (e.g., Biggs & Ivison 2008; Miettinen et al. 2017; Thomson et al. 2019), and emission lines such as [CII] (Gullberg et al. 2018; Litke et al. 2018), 12CO (Spilker et al. 2015; Chen et al. 2017; Tadaki et al. 2017b; Calistro Rivera et al. 2018; Dong et al. 2019), H2O (Apostolosvski et al. 2019), and Hz (Alaghband-Zadeh et al. 2012; Menéndez-Delmestre et al. 2013; Chen et al. 2017; Nelson et al. 2019). While these studies mostly focused on more IR luminous sources, these results suggest that the dust distribution at $z \sim 2$ could be significantly different than that in galaxies in nearby universe, and spatially resolved studies comparing various star formation tracers are needed in order to better understand the physics of star formation during the epoch when most of the massive elliptical galaxies seen in the nearby universe are formed (e.g., Lilly et al. 1999; Hickox et al. 2012; Toft et al. 2014; Simpson et al. 2014; Chen et al. 2016; Wilkinson et al. 2017).

This paper is motivated by Chen et al. (2017), in which we found that in a submillimeter galaxy (SMG), ALESS67.1, at $z = 2.12$ where we managed to gather sub-arcsecond UV-to-NIR continuum, FIR continuum, 12CO, and Hα, the size of FIR continuum is a factor of $\sim$4-6 smaller than that of all other emissions. Calistro Rivera et al. (2018) have extended the size comparison between FIR continuum and 12CO to a sample of four SMGs, finding that 12CO(J = 3 – 2) is larger than the FIR continuum by a factor of $> 2$. They propose that the size difference can be explained by temperature and optical depth gradients alone. In this paper we aim to extend the comparison between the FIR continuum and Hα to a larger sample of SMGs. In Section 2 we provide details of our sample selection and data. The analyses and measurements are presented in Section 3. We discuss the implications of our findings in Section 4 and the summary is given in Section 5. Throughout this paper we define the size to be the half-light radius. We assume the Planck cosmology: $H_0 = 67.8 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_M = 0.31$, and $\Omega_\Lambda = 0.69$ (Planck Collaboration et al. 2014).
Table 1. General information of the sample and the data

| ID          | R.A. ALMA [J2000;degree] | Decl. ALMA [J2000;degree] | AGN[a] | PSF ALMA, nat [arcsecond] | PSF ALMA, tap [arcsecond] | IFU   | IFU band | PSF IFU [arcsecond] |
|-------------|--------------------------|---------------------------|--------|---------------------------|---------------------------|-------|----------|---------------------|
| ALESS17.1   | 53.030410                | −27.855765                | X-ray  | 0.17×0.15                 | 0.66×0.62                 | SINFONI H | 0.65     |
| ALESS66.1   | 53.383053                | −27.902645                | No     | 0.17×0.13                 | 0.47×0.45                 | SINFONI K | 0.48     |
| ALESS67.1   | 53.179981                | −27.920649                | X-ray  | 0.18×0.15                 | 0.66×0.62                 | SINFONI HK | 0.66     |
| ALESS75.1   | 52.863303                | −27.930928                | IR     | 0.17×0.12                 | 0.57×0.54                 | SINFONI HK | 0.56     |
| AS2UDS292.0 | 34.322638                | −5.2300513                | X-ray  | 0.22×0.19                 | 0.46×0.42                 | KMOS K    | 0.46     |
| AS2UDS412.0 | 34.422392                | −5.181028                 | No     | 0.25×0.23                 | 0.56×0.52                 | KMOS K    | 0.55     |

(a) The AGN classification in X-ray is based on catalog matching: ALESS SMGs are matched to the Chandra 7 Ms catalog and classified as AGN based on the criteria set in Luo et al. (2017). The AS2UDS SMGs are matched to the Chandra X-UDS catalog (Kocevski et al. 2018) with a simple luminosity cut of $L_{2-10\text{keV}} > 3 \times 10^{42} \text{ erg s}^{-1}$, which is one of the criteria used in Luo et al. (2017). The steep slope in mid-infrared has suggested that ALESS75.1 is an IR AGN (Simpson et al. 2014; Stanley et al. 2018).

Fig. 1. Two dimensional Hα maps of our sample SMGs (Table 1) with a size of 25×25 kpc and a color stretch from zero to 99.5% of the peak. The solid and the dashed contours starting from 3σ are overlaid on top to show two versions of the ALMA 870 µm continuum, respectively; One produced using natural weighting, resulting in ~0′′.2 resolution, and the other tapered to ~0′′.5 resolution, matching to the resolution of the Hα images. The resolution beams in sizes of FWHM are plotted in the bottom corners and the exact sizes are given in Table 1. White and green crosses mark the positions adopted as the centers of the curve-of-growth analyses, for 870µm continuum and Hα, respectively. These positions are centroids of the best-fit ellipses to the isophotes of the corresponding 2D images, with the details described in Section 3. Sources that are identified to host an AGN are marked with an asterisk after the ID. The nearby foreground quasar next to ALESS66.1 is marked as a red dot. We find that the rest-frame FIR emissions appear to be smaller in scale than Hα in most sources.

2. Sample, data, and reductions

2.1. Sample

Our sample of six SMGs is drawn from two parent SMG samples. One is the ALESS sample (Hodge et al. 2013; Karim et al. 2013), obtained from a Cycle 0 ALMA 850 µm follow-up survey targeting a flux-limited sample of 126 submillimeter sources detected by a LABOCA (Siringo et al. 2009) 870 µm survey in the Extended Chandra Deep Field South (ECDFS) field (LESS survey; Weiß et al. 2009). These sources were subsequently...
observed at a higher angular resolution with ALMA (Hodge et al. 2016, 2019). The other is the AS2UDS sample (Simpson et al. 2017; Stach et al. 2018, 2019), based on a Cycle 1,3,4,5 ALMA 850µm follow-up program of all 716 > 4σ submillimeter sources uncovered by the SCUBA-2 850µm legacy survey in the UKIDSS-UDS field (Geach et al. 2017).

To compare the morphology of FIR continuum and Hα, in particular the measurement of sizes, it requires spatially resolved observations, which for SMGs typically means observations taken at ≤0′′5 (e.g., Simpson et al. 2015; Alaghband-Zadeh et al. 2012). Therefore for the selection of galaxies from ALESS and AS2UDS for this study we require, firstly, that targets have ≤0′′5 angular resolution ALMA band 7 continuum imaging, which has a matched or better spatial resolution to the seeing-limited Hα data so it allows direct comparisons in spatial distributions between cold dust continuum and Hα. Majority of the AS2UDS SMGs satisfy this criterion (Stach et al. 2019) and for ALESS SMGs we consider the ones published in Hodge et al. (2016) and an extra sample obtained through the program 2016.1.00735.S (PI: C. M. Harrison).

The second step is to based on the positions of these SMGs search the VLT archive for the existing IFU (SINFONI or KMOS) observations. We reduce the archival data following the methods described in the next section. To allow creations of two-dimensional intensity maps we keep the SMGs that have high signal-to-noise ratio Hα detection (but remove obvious broad line active galactic nuclei; BLAGN), corresponding to a typical flux density of ~10⁻¹² erg s⁻¹ cm⁻². While the archival data have been taken by different programs so it is difficult to assess the potential selection biases, we note that the Hα flux density distribution (5 × 10⁻¹⁷ – 3 × 10⁻¹⁶ erg s⁻¹ cm⁻²) of our sample SMGs follows that reported in the literature on other SMG samples (Swinbank et al. 2004; Casey et al. 2017). Under these two criteria we have obtained four ALESS and two AS2UDS SMGs, and their basic properties are given in Table 1.

Based on the SED analyses shown later using the MAGPHYS code, we find that these six SMGs have a median dust mass of log(M_dust)=8.9 M_☉, a median stellar mass of log(M_*)=11.2 M_☉ and a median SFR of log(SFR)=2.4 M_☉ yr⁻¹, meaning they are on average located on the upper part of the massive end of the SFR-M, main sequence at z ~ 2, which is consistent with the behaviour of the general SMG population (da Cunha et al. 2015).

2.2. SINFONI and KMOS IFU

The SINFONI-IFU data were taken for the four ALESS sources between October 2013 and December 2014 under the program IDs 091.B-0920 and 094.B-0798. We used H-, K-, and HK-band to observe ALESS17.1, ALESS66.1, and both ALESS67.1 and ALESS75.1, respectively, covering the [N ii]/Hα lines in all four sources and the [O iii]/Hβ lines in the last two. The spectral resolution is R > 1500, sufficient to separate Hα and the two [N ii] lines. The data were reduced using the esorex (ESO Recipe Execution Tool) (Freudling et al. 2013) pipeline, with additional custom routines applied to improve the sky subtraction. Solutions for flux calibration were derived using the IRAF routines.
The K-band KMOS data on AS2UDS SMGs were taken by the KMOS3D survey (Wisnioski et al. 2015) under the program IDs 993.A-0079 and 096.A-0025. The data reduction primarily made use of SPARK (Software Package for Astronomical Reduction with KMOS; Davies et al. 2013), implemented using the esorex package. In addition to the SPARK recipes, custom python scripts were run at different stages of the pipeline and are described in detail in Turner et al. (2017). Standard star observations were carried out on the same night as the science observations and were processed in an identical manner to the science data, which were used for flux calibration and PSF generation. Sky subtraction was enhanced using the SKYTWEAK option within SPARK (Davies 2007), which counters the varying amplitude of OH lines between exposures by scaling families of OH lines independently to match the data.

The astrometry of both the SINFONI and the KMOS data was corrected by aligning the continuum of the IFU cube to the corresponding ground-based imaging, including TENIS K-band (Hsieh et al. 2012) or MUSYC H-band in CDF-S (Taylor et al. 2009), and UKIDSS K-band (Lawrence et al. 2007) in UDS, which was first aligned to the GAIA DR2 catalog (Gaia Collaboration et al. 2018) based on sources with $R = 15 - 20$ mag (in AB). By doing so we found a significant systematic shift to the north in declination of the ground-based imaging in CDF-S with respect to the GAIA sources by $\sim 0\farcs3 \pm 0\farcs1$, consistent with similar findings in the literature (e.g., Xue et al. 2011; Dunlop et al. 2017; Luo et al. 2017; Scholtz et al. 2018). No systematic offset is found in UDS imaging. Assuming the ALMA astrometry aligns with GAIA DR2, the precision of astrometry of the IFU data derived through this exercise is $< 0\farcs2$ (around one pixel of the IFU data).

### 2.3. ALMA 870 $\mu$m continuum

The ALMA data of ALESS17.1, ALESS67.1 and the two AS2UDS SMGs have been published and described in detail in Hodge et al. (2016), Chen et al. (2017), and Stach et al. (2018). To present the data self-consistently, we re-analyse the data by first creating the calibrated measurement set using the pipeline reduction scripts provided by the ALMA archive, with a corresponding casa version used to generate the scripts. ALESS66.1 and ALESS75.1 were observed in Cycle 4 as a comparison sample for testing the size difference between SMGs with or without detectable AGN (Project ID: 2016.1.00735.S). We again use the pipeline reduction script to create the calibrated measurement set under casa version 4.7.2. All ALMA data were tuned to the default band 7 continuum observations centered at 344 GHz/870 $\mu$m, with 4 $\times$ 128 dual polarization channels over the 8 GHz bandwidth. At this frequency, ALMA has a 17$''$:5 primary beam in FWHM.

We then make two sets of images; One is created using natural weighting and the other tapered to a spatial resolution matched to the H$\alpha$ data. Both sets of images are deconvolved using the clean algorithm, and circular regions with 1$''$:5 radius centered at the SMGs are cleaned down to 2 $\sigma$. The typical angular resolution under natural weighting is $\sim 0\farcs2$, and $\sim 0\farcs5$ for the tapered images (Table 1), and the corresponding depths in r.m.s. are 30-70 $\mu$Jy beam$^{-1}$ and 60-300 $\mu$Jy beam$^{-1}$, respectively.

### 3. Analyses and measurements

#### 3.1. SINFONI and KMOS IFU

For spectral analyses we use the code detailed in Chen et al. (2017) to fit both the emission lines and the near-infrared (NIR) continuum. In short, the code first performs fits to each spectrum with various models including continuum and different combinations of the H$\alpha$, [N$\text{II}$], and [S$\text{II}$] lines. It then selects the best model based on the Akaiake information criterion, in particular the version that is corrected for the finite sample size (AICc; Hurvich & Tsai 1989). Finally, a model fit with line components is considered significant if the fit, compared to a simple continuum-only model, has a lower AICc and provides a $\chi^2$ improvement of $\Delta \chi^2 > 16$ for an H$\alpha$-only model, and an additional improvement of $\Delta \chi^2 > 9$ for each additional line. The fits are weighted against the sky spectrum provided by Rousselot et al. (2000) and when calculating $\chi^2$ the wavelength ranges corresponding to the skylines are masked. The velocity dispersion is corrected in quadrature for instrumental broadening. The errors are derived using Monte Carlo simulations; We create fake spectra by injecting the model profile into spectra extracted from randomly selected regions of the data cube with the same circular aperture used for the detection spectrum. The errors are then obtained from the standard deviations between the fit results and the input model.

To measure the total line flux densities, we employ the curve-of-growth analyses, in which the integrated line flux densities are measured with increasing size of circular apertures. The total line flux densities are then obtained at a certain radius beyond which the line flux densities do not significantly increase, so hitting a plateau. This approach is independent of any 2D surface brightness models and also adopted in some recent work in the literature (e.g., Chen et al. 2017; Förster Schreiber et al. 2018). To do such analyses, first the centroid of the circular aperture needs to be determined. We define the centers of H$\alpha$ curve-of-growth analyses to be the centroids of the ellipses best fit to the isophotes of the two dimensional (2D) emission line maps, specifically the isophotes that have their sizes matched to the corresponding spatial resolution. The 2D emission line maps are created by performing line fitting on spectra extracted from each individual pixels, with an adaptive binning approach up to 5x5 pixels depending on the signal-to-noise ratios (e.g., Swinbank et al. 2006; Chen et al. 2017). In pixels where the fitting still fails after 5 $\times$ 5 binning to give an adequate S/N, we leave the pixel blank without a fit. The caveat of this approach is that the signals are weighted toward the higher S/N pixels. The outcome of the curve-of-growth analyses is plotted in Figure 2, the measurements are given in Table 2, and the 2D emission line maps are shown in Figure 1.

The H$\alpha$ sizes are measured in two ways. First is to measure the sizes in the curve-of-growth analyses shown in Figure 2. We use a spline linear fit to the measurements and derive the radius, along with the uncertainties, that corresponds to half of the size.

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1. The ideal way to monitor the PSF for SINFONI is to request the PSF standard observations but they do not exist in any of the data set used. However we checked the recorded seeing conditions between the standard stars and the science targets and found they agree to $\sim 15\%$ without a significant systematic offset.

2. Equivalent to an S/N $> 4\sigma$ assuming Gaussian noise and that the noise is not correlated among wavelength channels.
normalized flux density. The same procedure is applied on the PSFs, and by subtracting the PSF sizes from the measured sizes in quadrature we derive the deconvolved, intrinsic sizes. We apply the same analyses on both Hα and the 870 μm continuum. The results are given in Table 2.

The second method is to use galfit (v3.0.5; Peng et al. 2010) to conduct single Sérsic profile fits. The basic procedure closely follows Chen et al. (2015). Before fitting, we first convert the 2D emission line intensity maps to conduct single Sérsic profile fits. The basic procedure closely follows Chen et al. (2015). Before fitting, we first convert the 2D emission line intensity maps to conduct single Sérsic profile fits. The basic procedure closely follows Chen et al. (2015). Before fitting, we first convert the 2D emission line intensity maps to conduct single Sérsic profile fits. The basic procedure closely follows Chen et al. (2015). Before fitting, we first convert the 2D emission line intensity maps to conduct single Sérsic profile fits. The basic procedure closely follows Chen et al. (2015). Before fitting, we first convert the 2D emission line intensity maps to conduct single Sérsic profile fits. The basic procedure closely follows Chen et al. (2015). Before fitting, we first convert the 2D emission line intensity maps to conduct single Sérsic profile fits. The basic procedure closely follows Chen et al. (2015). Before fitting, we first convert the 2D emission line intensity maps to conduct single Sérsic profile fits. The basic procedure closely follows Chen et al. (2015). Before fitting, we first convert the 2D emission line intensity maps to conduct single Sérsic profile fits. The basic procedure closely follows Chen et al. (2015). Before fitting, we first convert the 2D emission line intensity maps to conduct single Sérsic profile fits. The basic procedure closely follows Chen et al. (2015). Before fitting, we first convert the 2D emission line intensity maps to conduct single Sérsic profile fits. The basic procedure closely follows Chen et al. (2015).

The results are given in Table 2 and they are consistent with the fact that the FIR continuum is not circular in morphology but elongated (Figure 1).

4. Discussions

4.1. Size measurements

In Section 3 we present sizes for both the FIR continuum and Hα. Now we compare our results to those in the literature. Note that while we show that all methods of deriving sizes reach consistent results, for uniformity from now on we adopt the values obtained from the curve-of-growth method, which is model independent and allows consistent measurements on both data sets.

Uncertainties are given in the parentheses.

Notes.

(a) Total 870 μm continuum flux density estimated from Gaussian fits in the visibility domain. (b) Total Hα flux density. (c) Half-light radius in major axis at 870 μm obtained from casa fitting in the visibility domain. (d) Half-light radius at 870 μm obtained from the curve-of-growth analyses based on the ALMA continuum imaging. (e) Hα half-light radius in major axis obtained using galfit based on the 2D emission line intensity maps. (f) Hα half-light radius obtained from the curve-of-growth analyses based on the IFU cubes. (g) Hα over 870 μm continuum size ratio in which the sizes from the curve-of-growth method are adopted.

Table 2. FIR continuum and Hα measurements of our sample

| ID       | redshift | $F_{870}^{a}$ [mJy] | $F_{\text{Ha}}^{b}$ [1E-16 erg s$^{-1}$ cm$^{-2}$] | $r_{e,\text{maj,870,uv}}^{c}$ [kpc] | $r_{e,\text{Ha,galfit}}^{d}$ [kpc] | $r_{e,\text{Ha,cog}}^{e}$ [kpc] | $r_{e,\text{ratio}}^{f}$ |
|----------|----------|----------------------|---------------------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|----------------------------|
| ALESS17.1| 1.5392(2) | 8.2(0.2)             | 0.6(0.2)                                    | 1.7(0.1)                          | 4.5(0.5)                          | 3.0(0.6)                          |
| ALESS66.1| 2.5534(2) | 2.7(0.1)             | 1.5(0.3)                                    | 2.2(0.2)                          | 3.2(0.5)                          | 1.3(0.3)                          |
| ALESS67.1| 2.1228(6) | 3.7(0.2)             | 2.6(0.4)                                    | 1.8(0.3)                          | 5.7(0.5)                          | 3.4(0.7)                          |
| ALESS75.1| 2.5468(3) | 2.6(0.2)             | 3.4(0.5)                                    | 1.9(0.2)                          | 4.0(0.6)                          | 2.1(0.3)                          |
| AS2UDS292.0| 2.1822(1) | 3.1(0.4)             | 1.0(0.2)                                    | 2.0(0.7)                          | 3.9(0.3)                          | 1.8(0.5)                          |
| AS2UDS412.0| 2.5217(8) | 3.7(0.2)             | 0.5(0.2)                                    | 1.5(0.1)                          | 2.7(0.3)                          | 1.5(0.8)                          | 1.1(0.5) |

References:

Chen et al. (2015), Hodge et al. (2016), Molina et al. (2017), Alaghband-Zadeh et al. (2012), Ikarashi et al. (2015), Spilker et al. (2015), Tadaki et al. (2017a), Fujimoto et al. (2018), Simpson et al. (2015), Hodge et al. (2016), Molina et al. (2017), Alaghband-Zadeh et al. (2012), Molina et al. (2017), Forster Schreiber et al. (2018).

3 The disk model in casa is not an exponential disk but an uniformly bright disk.

The median size derived from the one dimensional curve-of-growth method ($r_{e,870}\text{cog}$) is 1.9 ± 0.2 kpc, which is consistent within errors with the one in major axis based on Gaussian fits in the $\alpha$-plane. The slightly larger sizes in major axis over the one from curve-of-growth (median $r_{e,\text{maj,870,uv}}/r_{e,\text{870,cog}} \approx 1.1$) are consistent with the fact that the FIR continuum is not circular in morphology but elongated (Figure 1).
the size of $\mathrm{H}\alpha$ agrees with that of optical continuum (Förster Schreiber et al. 2018) and the size of optical continuum positively correlates with the stellar mass (e.g., van der Wel et al. 2014), this discrepancy can be explained by the fact that our sample SMGs are more massive ($\sim 10^{11} \, M_\odot$) than that of the other galaxy samples ($\sim 10^{10} \, M_\odot$).

![This work: $z=1.25$ starburst](image)

Fig. 3. A plot showing the comparison between the sizes of $\mathrm{H}\alpha$ and those of the rest-frame FIR continuum. Our sample SMGs are plotted in filled symbols along with their IDs, which have their field names removed for clarity. Sources that are identified to host an AGN are marked with an asterisk after the ID. We also plot in an empty symbol the measurements of a starburst galaxy at $z=1.25$ recently presented by Nelson et al. (2019). Based on our sample SMGs we find on a median $\mathrm{H}\alpha$-to-FIR size ratio of $2.0 \pm 0.4$ with a bootstrapped uncertainty.

The sizes of FIR continuum and $\mathrm{H}\alpha$ of our sample SMGs, as well as one dusty galaxy at $z=1.25$ that also has size measurements in both FIR continuum and $\mathrm{H}\alpha$(Nelson et al. 2019), are compared in Figure 3, in which a clear size difference is shown. In all cases $\mathrm{H}\alpha$ emission appears larger than the FIR continuum (half differ by $>3\sigma$), with a maximum $\mathrm{H}\alpha$-to-FIR size ratio of over three. On average, the size difference in our sample is a median factor of $2.0 \pm 0.4$ with a bootstrapped uncertainty.

Interestingly we find that SMGs hosting AGN tend to have larger size ratios, prompting the question of whether AGN is driving the larger $\mathrm{H}\alpha$-to-FIR size ratios. For the three X-ray AGN we can infer the expected $\mathrm{H}\alpha$ luminosities contributed by the AGN by adopting the $L_{\mathrm{X}} - L_{\mathrm{H}\alpha}$ correlation deduced by Ho et al. (2001) based on samples of nearby AGN, and we find that $\leq 10\%$ of the measured $\mathrm{H}\alpha$ luminosities are contributed by AGN. In addition, the low [NII]-to-$\mathrm{H}\alpha$ ratios in all of our sample SMGs, in particular the outskirts, suggest that the ionizing conditions are consistent with those of $\mathrm{H}\alpha$ regions, and that $\mathrm{H}\alpha$ can be mainly attributed to star formation and not AGN. Finally, there is currently no evidence, including our sample, suggesting that the FIR continuum sizes depend on the presence of an AGN (e.g., Harrison et al. 2016).

On the other hand, recently a similar study by Scholtz et al. (2020) on a sample of eight X-ray selected AGN at $z \sim 2$ with strong $\mathrm{H}\alpha$ and [OIII] lines also found a similar $\mathrm{H}\alpha$-to-FIR size ratio of $2.3 \pm 0.3$. This evidence could suggest that somehow AGN is driving the larger $\mathrm{H}\alpha$ sizes, or it could be that this is a general feature of FIR luminous galaxies at $z \sim 2$ and the current studies are biased toward galaxies hosting AGN because of their bright-ness of strong optical lines. Nevertheless, a systematic study on a larger sample, especially including more FIR luminous sources without hosting AGN, is clearly needed to investigate this further.

The larger $\mathrm{H}\alpha$ size over FIR continuum in $z \sim 2$ dusty star-forming galaxies is somewhat expected according to recent studies in the literature comparing either FIR and rest-frame optical continuum or $\mathrm{H}\alpha$ and rest-frame optical continuum. For example, Hodge et al. (2016) found that the rest-frame optical continuum of their sample of ALESS SMGs is about three times larger than the FIR continuum. This size difference of a factor of 2-3 is almost universally observed in both other similarly FIR-luminous galaxies (e.g., Barro et al. 2016; Elbaz et al. 2018) and less FIR-luminous star-forming galaxies at $z \sim 2$ (e.g., Tadaki et al. 2017a; Fujimoto et al. 2018).

On the other hand, using AO-aided SINFONI IFU data that are matched in spatial resolution to the HST imaging, Förster Schreiber et al. (2018) show that on average the $\mathrm{H}\alpha$ size of their $z \sim 2$ massive star-forming galaxies is identical to the rest-frame optical continuum. Chen et al. (2017) found a similar result on one SMG, ALESS67.1, which is included in our sample. Four of our sample SMGs have HST $H$-band imaging, and the results of the curve-of-growth analyses are plotted in Figure 2. On average we find a $\mathrm{H}\alpha$-to-optical size ratio of $1.0 \pm 0.1$.

All these results suggest that on average $\mathrm{H}\alpha$ is similar in size to the rest-frame optical continuum, and both are a factor of 2-3 larger than the FIR continuum. The much smaller size of FIR continuum compared to almost any other tracers, including molecular gas (e.g., Ginolfi et al. 2017; Chen et al. 2017; Calistro Rivera et al. 2018), challenges the typical assumption regarding the treatment of dust attenuation in the SED modeling (e.g., Simpson et al. 2017). In the following sections we investigate and discuss in detail some possible implications.

### 4.2. Star formation rates

There are a few possible implications of the size difference between FIR continuum, $\mathrm{H}\alpha$ and optical-to-infrared (OIR) continuum. We start with the measurements of star-formation rates. Note the UV-to-NIR photometry of ALESS66.1 is contaminated by a nearby quasar at $z=1.31$ (Simpson et al. 2014; Danielson et al. 2017). We therefore exclude it from the analyses from now on.

#### 4.2.1. Dust correction of $\mathrm{H}\alpha$

Under the assumption that the total star-formation rates can be estimated through either attenuation-corrected $\mathrm{H}\alpha$ or UV-to-FIR continuum photometry, one possible implication of the size difference has to do with the attenuation correction of $\mathrm{H}\alpha$-based SFRs, particularly in cases where FIR measurements are not available. To account for dust attenuation a typical approach is to assume a foreground dust screen, which is co-spatial in the projected sky with the underlying UV/optical star-formation tracers. This is one of the fundamental assumptions of some of the popular SED modeling involving corrections of dust attenuation, including HYPERZ (Bolzonella et al. 2000) and EAZY (Brammer et al. 2008). However with spatial mismatches between $\mathrm{H}\alpha$ and FIR continuum these assumptions need to be further examined and the possible impact needs to be understood.

To understand such an impact, if any, we first aim to compare the attenuation-corrected $\mathrm{H}\alpha$-based SFRs and the dusty SFRs derived from the total infrared luminosities. That is, instead of
adopting the energy-balance approach we model the UV-to-NIR and MIR-to-radio SEDs separately, so mimicking the traditional approach of deriving total SFRs without FIR measurements and then use the FIR-inferred SFRs to validate this approach. In principle, a significant size difference between dust and H$_\alpha$ regions may result in the attenuation-corrected H$_\alpha$-based SFRs being systematically lower than the dusty SFRs, or both measurements being uncorrelated, or both.

To obtain the attenuation-corrected H$_\alpha$ SFRs, the best approach is to also measure the H$_\beta$ luminosity and estimate the nebular attenuation through the Balmer decrement (e.g., Reddy et al. 2015). However H$_\beta$ is not available in all but a marginal detection from one SMG, ALESS75.1. To be able to apply a consistent methodology across the sample, alternatively we opt to use the stellar attenuation derived from the UV-to-NIR SED fitting. Further corrections on top of the stellar attenuation may need to be applied (e.g., Calzetti et al. 2000; Wuyts et al. 2013; Price et al. 2014).

To model the UV-to-NIR SEDs we use Hyperz (Bolzonella et al. 2000), a $\chi^2$ minimization code to fit a set of model SEDs on the observed photometry. The model SEDs are based on synthetic SED templates whose intrinsic shape is characterized by the star-formation history (SFH). The synthetic SEDs are further modified according to dust reddening, Lyman forest, and redshifts. The four synthetic SED templates considered are created with spectral templates of Bruzual & Charlot (2003), assuming solar metallicities, with different SFHs: a single burst (B), two exponentially decaying SFHs with timescales of 1 Gyr (E) and 5 Gyr (Sb), and constant star formation (C). The undetected photometric measurements are set to a flux of zero with uncertainties equal to 1 $\sigma$ of the limiting magnitude of that filter. We follow the Calzetti et al. (2000) law to allow total attenuation ($A_V$) between 0 to 5 in steps of 0.1. The age of the galaxy must be younger than the age of the Universe.

Our methodology is similar to that of Simpson et al. (2014), who also conducted Hyperz fitting on ALESS SMGs. However they did not have full spectroscopic redshift information. Therefore as a check we first compare our fitting results on the ALESS SMGs against those of Simpson et al. (2014), by allowing the redshift to vary between 0 and 6 in steps of 0.1. We confirm that we are able to reproduce their results. We then determine $A_V$ by setting the redshift range to the spectroscopic redshifts with uncertainties measured from H$_\alpha$. We find that under one synthetic SED template $A_V$ are always invariant within the spectroscopic redshift uncertainties (we adopt $\pm 3$ $\sigma$). However the variations become significant from template to template, namely they are affected by the SFHs adopted. We therefore perform fits by considering one SED template at a time and take all the $A_V$ values from fits that have $\Delta \chi^2 < 1$ from the lowest $\chi^2$. When deriving the dust-corrected SFRs we propagate the range of these $A_V$ values into the uncertainties. We find typical $A_V$ values of 1 to 3 for SED sampled down to the rest-frame UV, consistent with previous findings of SMGs (Takata et al. 2006; Wardlow et al. 2011; Simpson et al. 2014; da Cunha et al. 2015).

We now move on to the fitting of the FIR SEDs. We adopt the approach of template fitting. In particular we use the library of 185 template SEDs constructed by Swinbank et al. (2014), who included local galaxy templates from Chary & Elbaz (2001), Rieke et al. (2009) and Draine et al. (2007), as well as the SEDs of the well-studied high-redshift starbursts SMM J21350102 ($z = 2.32$) and GN20 ($z = 4.05$) from Ivison et al. (2010) and Carilli et al. (2011), respectively. The MIR-to-radio photometry of the ALESS SMGs, including MIPS 24, PACS 70 and 160 $\mu$m, SPIRE 250, 350, and 500 $\mu$m, ALMA 870 $\mu$m, and VLA 1.4 GHz, are derived by Swinbank et al. (2014). The same methodology is applied to the AS2UDS SMGs (Stach et al. 2019). We fit the MIR-to-radio photometry using $\chi^2$ minimization and adopt the spectroscopic redshifts measured by our IFU fitting.
observations. We then derive the infrared luminosity by integrating the best-fit template SED, as well as all acceptable SEDs based on their \( \chi^2 \) values, over the rest-frame 8-1000 \( \mu \)m range.

Having the fitting results in hand, we estimate the star-formation rates based on \( H\alpha \) and infrared luminosities by adopting the calibration provided by Kennicutt & Evans (2012)\(^4\). We plot the results in Figure 4. First we find that the \( H\alpha \)-based SFRs without attenuation correction are on average a factor of \( 21 \pm 15 \) in median (with bootstrap error) lower than infrared-based SFRs. Similar discrepancies have been reported in other SMG samples (Swinbank et al. 2004; Casey et al. 2017). We then correct the \( H\alpha \) luminosities using the stellar attenuation via \( L_{H\alpha} = L_{H\alpha, obs} \times 10^{\beta_{H\alpha}/V} \), in which \( A_{V, star} \) is obtained through the UV-to-NIR hyperz fitting. After correcting for dust attenuation, the infrared SFRs are still systematically higher, but now by a factor of 4 ± 2.

The systematically lower \( H\alpha \)-based SFRs after correcting for stellar attenuation suggests that, given the assumption that the total SFRs can be obtained either from infrared luminosity or attenuation-corrected \( H\alpha \), an additional correction on top of the stellar attenuation is needed for \( H\alpha \). On the other hand, if the discrepancy persists after further corrections, the aforementioned assumption may be challenged and it could suggest that the bulk of the dusty star formation may not be traced through rest-frame optically detectable regions including \( H\alpha \) regions, as partly supported by our findings of size difference.

To assess the amount of further correction, we now look at the possible differences between nebular and stellar attenuation. Using the Balmer decrement, the comparison of the two has been extensively studied, in both local samples (Calzetti et al. 2000; Wild et al. 2011; Kreckel et al. 2013) and higher redshifts (Kashino et al. 2013; Price et al. 2014; Reddy et al. 2015; Theios et al. 2018). In particular, the seminal work of Calzetti et al. (2000) found that using a sample of local starbursting galaxies the nebular attenuation is larger with a relation of \( E(B-V)_{star} = 0.44 \pm 0.03 E(B-V)_{neb} \) and Kashino et al. found \( E(B-V)_{star} = 0.70 \pm 0.08 E(B-V)_{neb} \).

Given \( A_{V} = \kappa(\lambda)E(B-V) \) in which \( \kappa(\lambda) \) is the attenuation curve\(^5\), we deduce a total attenuation relation of \( A_{H\alpha} = 1.4 \pm 0.1A_{V, star} \) and \( A_{H\alpha} = 0.9 \pm 0.1A_{V, star} \) based on the result of Calzetti et al. (2000) and Kashino et al. (2013), respectively. We apply the relation to our measurements and plot the results in Figure 4.

Despite applying further corrections, the attenuation-corrected \( H\alpha \)-based SFRs still cannot account for all the SFRs revealed in the infrared, missing at least a median factor of \( 3 \pm 1 \) considering the most aggressive correction based on the Calzetti attenuation curve. The Spearman correlation coefficient is 0.6 (\( p = 0.2 \)) so the two SFRs appear possibly correlated among these five galaxies. However given the discrepancy between the two SFRs even after accounting for attenuation for \( H\alpha \), the correlation could be driven by the global properties of the galaxy such as gas fraction or the dynamical environment, instead of them tracing the same part of star-forming regions, which is partially supported by our findings of size difference between the two SFR traces. It is also possible that dust is spatially mixed with \( H\alpha \) regions, instead of acting as a foreground screen, and that dust column density reaches a level that \( H\alpha \) becomes optically thick, in particular in the central regions, so \( H\alpha \) does not reflect the full attenuation. Evidence of this possibility has been shown in studies of local (Ultra) Luminous Infrared Galaxies ((U)LIRGs), where the attenuation derived from Paα/Bry or Bry/Brγ in near-infrared is slightly higher than that derived from Balmer decrement (e.g., Piqueras López et al. 2013). Interestingly, for the local ULIRGs there is also evidence showing that their IR-based SFRs are higher than the attenuation-corrected, \( H\alpha \)-based SFRs, by a factor of 2-30 (García-Marín et al. 2009). In the next section we further investigate the reasons driving the mismatching SFRs, in particular the size difference between FIR continuum and \( H\alpha \).

4.2.2. Total star-formation rates

In Section 4.2.1 we discussed the implications due to the spatial mismatches between the FIR continuum, \( H\alpha \) emission, and optical continuum. In particular when considering SFRs, the attenuation corrected \( H\alpha \)-based SFRs are systematically lower than the IR-based SFRs. Given the total SFRs at high redshifts are frequently either derived from IR+UV or attenuation corrected \( H\alpha \) (e.g., Shivaei et al. 2016), the discrepancy merits further discussions. We explore two closely related issues: One on the attenuation correction, and the other about the spatial mismatches between the bulk of dust and the \( H\alpha \) regions.

On the attenuation correction, in order to align both SFRs, the correction needs to be about 50% more on top of the extra correction provided by Calzetti et al. (2000), which is similar to what was found by Wuyts et al. (2013). However such an aggressive correction based on the Balmer decrement has never been applied.

\(^4\) The conversion from infrared luminosities to SFRs heavily depends on the star-formation history, varying by a factor of around five given different star formation timescales (Calzetti 2013). Ideally one should adopt the conversion based on the best-fit SED template from hyperz. However as shown in previous studies of SMGs, the UV-to-NIR continuum tends to spatially offset from the FIR continuum (Chen et al. 2015; Hodge et al. 2016). Therefore the star-formation history derived from UV-to-NIR photometry likely does not reflect the true star-formation history in the dust regions emitting FIR continuum. The conversion from Kennicutt & Evans (2012) represents roughly the mean value of the possible range provided by Calzetti (2013). We therefore expect the uncertainty of the conversion due to unknown star-formation history contributes mostly to the scatter of the correlation, not the normalization.

\(^5\) The original relation found by Kashino et al. is \( E(B-V)_{star} = 0.83 \pm 0.1E(B-V)_{neb} \), which explicitly assumes a Calzetti attenuation curve on both Balmer decrement and stellar continuum. However Calzetti et al. (2000) adopted the Calzetti attenuation curve for the stellar continuum but a Milky Way attenuation curve on \( H\alpha \) (Cardelli et al. 1989). We therefore convert the Kashino et al. result based on the same assumption of the attenuation curves used in Calzetti et al. (2000).

\(^6\) The systematic lower \( H\alpha \)-based SFRs after correcting for stellar attenuation suggests that, given the assumption that the total SFRs can be obtained either from infrared luminosity or attenuation-corrected \( H\alpha \), an additional correction on top of the stellar attenuation is needed for \( H\alpha \). On the other hand, if the discrepancy persists after further corrections, the aforementioned assumption may be challenged and it could suggest that the bulk of the dusty star formation may not be traced through rest-frame optically detectable regions including \( H\alpha \) regions, as partly supported by our findings of size difference.

\(^7\) In our case UV-based SFRs are ~1% of IR-based SFRs so negligible.
be observed (e.g., Price et al. 2014). In fact, studies of $z \sim 2$ star-forming galaxies have found the opposite with significantly smaller values (e.g., Kashino et al. 2013; Reddy et al. 2015). We do note that these studies mostly focus on less obscured, lower stellar mass, and lower SFR galaxies in comparison with our sample SMGs. However if the IR-based and Hα-based SFRs were indeed to be matched, it would have suggested that globally the relation between the nebular $A_V$ and stellar $A_V$ is very different in the SMGs compared to that in the more typical star-forming galaxies. A more likely situation is that the bulk of the obscured star formation is not traced by either the Hα or stellar emissions, due to a combination of a few factors including global-scale size difference and very high obscuration in the central dusty regions. In the following we discuss further these two possibilities.

To quantify how much the global-scale size difference plays a role, one way is to estimate how much of the Hα-based SFRs originate from outside the bulk of dust as traced by the FIR continuum. Our data allow a simple one dimensional (1D) assessment. To do so, in Figure 5 we plot the SFR densities as a function of radial distances based on the FIR and Hα measurements. Since we do not have spatially resolved information of other FIR bands we assume that the IR-based SFR density profile follows the morphology of the observed 870$\mu$m emissions, as derived from the curve-of-growth analyses. That is, the IR-based SFRs in each radial bin is the fraction of the total 870$\mu$m flux in that bin multiplied by the total SFRs. This method effectively assumes a constant dust temperature and dust opacity, which is likely not true since evidence of negative temperature gradient (hot to cold from center to outskirts) has been found recently in SMGs (Calistro Rivera et al. 2018). However a negative gradient of dust temperature would mean an even more compact SFR density distribution.

For the Hα profiles, we simply differentiate the curve-of-growth results, convert the Hα luminosities to SFRs according to Kennicutt & Evans (2012), and adopt the stellar $A_V$ with a further correction to the nebular $A_V$ based on Calzetti et al. (2000), except for ALESS66.1, of which the OIR photometry is contaminated by a foreground quasar (Figure 1). For ALESS66.1 we plot the profile without correcting for attenuation. For clarity we only plot the bins that have $\geq 1\sigma$ measurements.

![SFR density profiles](image)

**Fig. 5.** The SFR density profiles based on the curve-of-growth analyses (Figure 2), which are deconvolved according to the PSF. Sources that are identified to host an AGN are marked with an asterisk after the ID. For the IR-based profiles we assume that they follow the morphology of the observed 870$\mu$m emissions, meaning the IR-based SFRs in each radial bin is the fraction of the total 870$\mu$m flux times the total SFRs. The Hα-based profiles are derived by differentiating the curve-of-growth results, converting the Hα luminosity to SFRs according to Kennicutt & Evans (2012), and adopting an attenuation correction of Calzetti et al. (2000), except for ALESS66.1, of which the OIR photometry is contaminated by a foreground quasar (Figure 1). For ALESS66.1 we plot the profile without correcting for attenuation. For clarity we only plot the bins that have $\geq 1\sigma$ measurements.
increase with a negative gradient of dust temperature. We also note that different centroids are adopted for 870 µm continuum and Hα in the curve-of-growth analyses (Figure 1), which has however a negligible impact such that the fraction would only increase by a maximum of 5% if the same centroids had been adopted. From this exercise, while it appears that in 1D profile the Hα-based SFRs are more extended relative to the FIR-based SFRs, the bulk of Hα-based SFRs spatially overlap with the FIR-based SFRs. That is, the size difference in the global scale between the FIR continuum and Hα is not the dominant factor that drives the mismatching SFRs estimated by these two SFR tracers. The dominant factors are likely linked to heavy dust attenuation in the central regions.

Fig. 6. UV-to-radio SEDs for each of our sample SMGs except ALESS66.1, of which the UV-to-NIR photometric measurements are contaminated by a foreground quasar Simpson et al. (2014). Sources that are identified to host an AGN are marked with an asterisk after the ID. The measurements are plotted as black points and the best-fit models from magphys, hyperz, and the IR templates compiled by Swinbank et al. (2014), are plotted as grey, blue, and red curves, respectively. For clarity we do not show the uncertainty however they are discussed in the text, including the fact that the IR luminosities estimated by the two methods agree with each other within the uncertainty. The insets are zoom-ins in the OIR regime from 0.3 to 10 µm in log-log scale. We find significant differences in higher LIR sources between the best-fit models of magphys and hyperz, and in all these discrepant cases the hyperz modeling provides a better fit with a lower $\chi^2$. 
Indeed, by estimating the hydrogen column density through dust masses and FIR continuum sizes, Simpson et al. (2017) found that by assuming a foreground screen of dust geometry, the averaged total attenuation in the central dusty regions of SMGs is $A_V = 540^{+30}_{-40}$, suggesting that effectively all of the optical-infrared (OIR) emission that is spatially coincident with the far-infrared emission region is completely extinguished by dust. In addition, in the most recent work by Hodge et al. (2019), at a spatial resolution of $\sim 500$ pc they found that the FIR continuum of SMGs becomes clumpy and structured in shapes of spiral arms, bars, and rings. In such a case the total attenuation of the dusty regions could exceed the values estimated by Simpson et al. (2017), suggesting that bulk of the dusty star formation as traced by FIR continuum is spatially decoupled from $H\alpha$ on sub-kpc scales. If we take the median value from Simpson et al. (2017), which is $A_V = 540$, and apply the correction to the $H\alpha$-based SFRs, the resulting SFRs would be on the order of $10^{7.43-540} \sim 10^{216}$ $M_\odot$ yr$^{-1}$, which is unrealistic. It would still be unrealistically high if we only apply this correction at the central regions where most of the dust is located.

On the other hand, another possibility could be that instead of acting as a foreground screen, the dust is mixed with the $H\alpha$ in this case the FIR continuum would not be spatially decoupled from $H\alpha$, but given the high column density $H\alpha$ is no longer optically thin therefore not reflecting the total attenuation. Both scenarios would lead to a significant underestimation of the total SFRs from $H\alpha$. More data on IR continuum along with the Balmer and even the Paschen lines with very high angular resolutions (< 0.1”), presumably from ALMA and ELT, should shed more light on this issue.

4.3. SED modeling and dust distribution

Another possible implication of size difference is the SED modeling, in particular those employing the energy-balance approach. We now discuss this aspect in detail.

4.3.1. Comparison to the energy balance approach

The spatial mismatch we see between dust and OIR emission may have implications for energy balance SED modeling. In particular, for our sample SMGs, one can imagine that because the majority of dust is not co-located with the OIR emissions, the attenuation estimated from OIR alone may be smaller than the attenuation derived from the energy balance approach. That is, the energy balance fitting may deduce a higher attenuation solution in OIR in order to provide a better fit to the FIR photometry, in particular for high luminosity sources. To test this possibility, we also model our UV-to-radio SEDs using the magphys code. We adopt the high-z edition, which includes the modeling in the radio bands, as well as the Lyman absorptions in the rest-frame UV from the intergalactic medium (da Cunha et al. 2015). We plot the best-fit models in Figure 6, along with the photometric measurements, and the fitting results of hyperz and those using the infrared templates.

We first compare the infrared luminosities estimated from the SED templates\(^8\) and those from magphys. We confirm that both values are statistically consistent with each other in all sources. We then turn to $A_V$, in which we find significant differences in some sources. As seen in Figure 6, ALESS67.1, ALESS75.1, and AS2UDS412.0 appear to have different best-fit models in the UV-to-NIR regime, although the fit from hyperz shows a better agreement with the data. Interestingly, in these three cases where the $A_V$ differ, the values obtained from magphys are all higher.

Note that given the different assumptions of the attenuation curves in these two codes, ideally the $A_V$ values from the UV-to-NIR regime should also be deduced from magphys by turning off the fitting of the MIR-to-radio part. Unfortunately the public version of magphys does not support such an option. However, the fact that the $A_V$ values are in excellent agreement with each other in ALESS17.1 and AS2UDS292.0, as expected from a good match shown in Figure 6, suggests that the systematic difference between the $A_V$ values can be neglected. We have also

\(^8\) The total infrared luminosity given by magphys is integrated over 3 to 1000 $\mu$m. We therefore adopt the same wavelength range to compute the total infrared luminosity from the best-fit SED templates.
tried to homogenize the two codes by running the Hyperz fitting using only the $\tau$-decay SFHs similarly adopted by Magphys, effectively removing the bursting SFH in our adopted method for Hyperz. We find that the output values vary within uncertainties and the conclusions remain unchanged. Since stellar mass is not one of the direct outputs from Hyperz we estimate the stellar masses by converting the absolute magnitude, which is one of the outputs from Hyperz, based on some estimates of mass-to-light ratios. In particular we take the H-band absolute magnitude from Hyperz and the mass-to-light ratios from Simpson et al. (2014) where the ratios were derived based on the Bruzual & Charlot (2003) simple stellar population models. We find that all but one (AS2UDS292.0) have their stellar mass estimates from the two codes in agreement with each other within uncertainties. The disagreement on AS2UDS292.0 is mainly caused, as expected, by the fact that the Hyperz fitting finds the best solution based on the bursting SFH. If we force a $\tau$-decay like fitting then the stellar mass estimated from Hyperz agrees with that from Magphys, with a little change in $A_V$ so again the conclusions are not sensitive to this change.

To further understand what causes the different $A_V$ values, in Figure 7 we first plot the $A_V$ ratios as a function of the size ratios between H$\alpha$ and the FIR continuum. Naively, one may expect that a better agreement in spatial distribution between dust and the OIR emissions would lead to a better agreement in $A_V$. That is, the more the sizes differ the more the $A_V$ differs. Interestingly we do not observe such a trend. Instead, we find a more prominent correlation between the $A_V$ ratios and the total infrared luminosity (Figure 7). While a larger sample is clearly needed to confirm, this correlation may suggest that indeed the energy balance approach deduces a higher $A_V$ in cases of high infrared luminosity, sacrificing a poorer fit in UV-to-NIR in return for an overall smaller $\chi^2$ value.

It is understandable that the discrepancy is the largest toward the higher infrared luminosity end, especially when the infrared luminosity is so high that the best-fit UV-to-NIR models cannot account for it. On the other hand, the more interesting question is perhaps why the $A_V$ values agree in the lower infrared luminosity end, despite the spatial mismatches. Based on da Cunha et al. (2008, 2015), Magphys adopts a two-component model (birth cloud and diffuse ISM) to describe the attenuation of stellar emission at the UV-to-NIR regime. Since the UV-to-NIR emissions largely originate from the stars in the birth clouds, the model, and some variations based on it, can explain most of the observational results regarding the dust distribution and the postulated three-component model. In addition, the fractional distribution between the birth clouds and the diffuse ISM can explain some correlations between the galaxy properties (SFR, stellar mass, and specific SFR) and the ratio of nebular to the stellar $A_V$ (e.g., Wild et al. 2011; Price et al. 2014; Reddy et al. 2015).

As briefly mentioned in the previous section, it is normally perceived that there are in general two main components for dust distribution (or attenuation); the diffuse ISM which encompasses mostly older stars and older star-forming regions revealed by the UV radiation, and the birth clouds tracing mostly HII regions where more intensive and younger star formation occurs. This is the essential assumption some of the SED models adopt, including those employ the energy balance approach (e.g., Magphys and Cigale). The advantage of this model, and some variations based on it, can explain most of the observational results regarding the different attenuation observed between H$\alpha$ and the stellar continuum. For example, the generally higher color excess of H$\alpha$ compared to that of stellar continuum is a natural consequence of this model. In addition, the fractional distribution between the birth clouds and the diffuse ISM can explain some correlations between the galaxy properties (SFR, stellar mass, and specific SFR) and the ratio of nebular to the stellar $A_V$ (e.g., Wild et al. 2011; Price et al. 2014; Reddy et al. 2015).

However, the two-component schematic model is built purely based on the OIR data, without the observational knowledge of the spatial distribution of dust. Through the analyses in Section 4.2.2, our data on the six SMGs suggest that the model becomes incomplete once the spatially resolved FIR data are considered, namely the majority of the dust attenuation cannot be traced via H$\alpha$ or OIR continuum only. A scenario that involves a third component, a centrally concentrated, extremely dusty component, appears more appropriate (Figure 8). Most of this third component of high dust concentration has a low filling factor and is likely not reflected by the rest-frame OIR and H$\alpha$.

Although this new scenario is based on the data of the six SMGs, it is also supported by other studies in the literature on
OIR-selected galaxy samples; For example, even having spatially resolved estimates of dust attenuation, Nelson et al. (2019) found insufficient correction of their Hα SFR in the central regions of a dusty galaxy at \( z = 1.25 \), resulting also in a mismatch between the Hα SFR density profile and that of the IR SFRs. Adding this component mitigates the tension between the \( A_V \) derived from OIR photometry only and that from the UV-to-radio energy balance modeling. It also naturally explains the mismatch between the Hα-based SFRs and IR-based SFRs on our sample SMGs. While we are lacking the measurements of nebular attenuation through Balmer decrement to completely verify this scenario on our sample SMGs, recent study by Scholtz et al. (2020) on a sample of eight ALMA-detected, X-Ray selected AGN confirm that in six of their AGN that have constraints of Balmer decrement, the nebular \( A_V \) values are indeed all larger than the stellar \( A_V \) values. Together with the fact that they also find a similar FIR continuum to Hα size ratio, the results of Scholtz et al. (2020) support the three-component model.

While SMGs can be located on or above the massive-end \(( \sim 10^{11} \, M_\odot) \) of the main sequence (e.g., Michałowski et al. 2012; da Cunha et al. 2015; Michałowski et al. 2017), due to their low space density the contribution of SMGs to the total cosmic star formation rate density is about 10-30% (Barger et al. 2012; Swinbank et al. 2014; Cowie et al. 2017). Therefore if the three-component model were to be generalized to the other galaxies at \( z \sim 2 \), perhaps a more interesting question to ask is to see if typical \( z \sim 2 \) star-forming galaxies that dominate the cosmic SFR density, and are on average less luminous in infrared have a similar FIR-to-Hα spatial disparity? A few studies in the literature may give us some hints.

Through FIR measurements of both individual galaxies and stacked images of their ALMA data, it has been found that on average galaxies at \( z \sim 2 \) are smaller if they have lower infrared luminosities \(( \sim 10^{12} \, L_\odot \) so SFR\( \sim 100 \, M_\odot \) yr\(^{-1}\); Tadaki et al. 2017a; Fujimoto et al. 2017, 2018). In addition, they also found that the FIR sizes are a factor of 2-3 smaller than the rest-frame optical sizes for galaxies with lower infrared luminosities. In the meantime, using AO-aided SINFONI observations, Förster Schreiber et al. (2018) found that in their sample of \( z \sim 2 \) star-forming galaxies that have a wide range of stellar masses \((2 \times 10^9 - 3 \times 10^11 \, M_\odot \), median \( 2 \times 10^10 \, M_\odot \) and SFRs \((10-650 \, M_\odot \) yr\(^{-1}\), median \( 80 \, M_\odot \) yr\(^{-1}\)), the stellar sizes are consistent with the Hα sizes to within 5% on average. These points of evidence suggest that a similar spatial disparity between FIR continuum and Hα and OIR continuum may also exist in star-forming galaxies with infrared luminosity less than the SMGs. If true, the three-component dust model may be applicable to the massive star-forming galaxies at \( z \sim 2 \) in general.

5. Summary

Using data from ALMA and near-infrared IFUs, we study the two-dimensional distributions of FIR continuum and Hα for a sample of six \( z \sim 2 \) SMGs. The objectives are to study their relative distributions and sizes, and investigate the impact of the results on issues such as the estimated star-formation rates, dust correction, dust distribution, and the SED modeling. We summarize our findings in the following:

1. The sizes of Hα are significantly (\( > 3 \sigma \)) larger than those of the FIR continuum in half of our sample SMGs (Figure 3). Across the sample the Hα sizes are a median factor of 2.0 \( \pm 0.4 \) larger than the FIR sizes.

2. We find that the observed Hα-based SFRs are systematically lower than the IR-based SFRs by a median factor of 20 \( \pm 15 \), and the factor is 4\( \pm 2 \) with attenuation correction applying the stellar \( A_V \) to Hα. By adopting the most extreme attenuation correction provided by Calzetti et al. (2000), the difference is still a factor of 3 \( \pm 1 \) (Figure 4).

3. By plotting the one-dimensional SFR density profiles (Figure 5) we find that less than 50% of the Hα emissions come from outside the radii spanned by the dusty star-forming regions as traced by the FIR continuum. This is therefore not sufficient in explaining the differences found between Hα-based SFRs and the IR-based SFRs. Given the expected high attenuation in the central dusty regions, we postulate that the majority of the obscured star formation is not reflected through the extinction of OIR emissions including Hα. It could be because that, in the scenario of foreground screen of dust, the FIR continuum and OIR emissions are spatially decoupled due to extremely high \( A_V \) (>100). It could also be, in the opposite scenario of dust mixing with stars, because of the OIR emissions becoming optically thick due to high column density. A mixture of both scenarios is also possible.

4. To understand the impact of spatial mismatches on the energy balance SED modeling, we compare the \( A_V \) values derived from hyperz using the OIR photometry alone and those from magphys. We find that the \( A_V \) values from magphys are significantly higher in two SMGs (out of five; one source is excluded due to foreground contaminations), where the two have the highest IR luminosities among the sample. This suggests that the energy balance approach deduces a higher \( A_V \) to account for the extra IR luminosities. For the three SMGs in which the \( A_V \) values agree, we postulate that the contribution of the IR emissions from the birth clouds could be unrealistically high.

5. Finally, considering the observed morphologies of Hα, OIR and FIR continuum, together with our findings about SFRs and \( A_V \), we postulate that the dust distributions in SMGs, and possibly also in less IR-luminous \( z \sim 2 \) star-forming galaxies, can be decomposed into three components; the diffuse ISM component obscuring the older stellar populations, the more obscured young star-forming Hı regions, and the heavily obscured central regions with low filling factor in which the bulk of attenuation cannot be reflected through Hα or OIR continuum.

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9 http://www.astropy.org
