Abraham Model Descriptors for Melatonin; Prediction of Solution, Biological and Thermodynamic Properties

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Abstract
Literature solubilities have been used to obtain properties or descriptors of melatonin. These indicate the chemical nature of melatonin: it is dipolar and has moderate hydrogen bond acidity and hydrogen bond basicity. The descriptors can be combined with equations that we have previously constructed to estimate water–solvent partition coefficients and solubilities in a huge number of organic solvents. In the same way, a range of biological properties can be estimated. These include blood–tissue partitions, water–skin partition and permeability through skin.

Keywords Melatonin · Hydrogen bonding · Solubilities · Linear free energy relationships · Biological properties

1 Introduction
Melatonin (CAS 73-31-4) is a natural hormone found in plants and animals, world-wide. In humans and animals it controls the sleep-wake circadian rhythm, and functions as an antioxidant and in plants it is involved in growth and in photosynthesis. The structure of melatonin is shown in Fig. 1. Melatonin supplements are widely used to combat sleep disorders. Surprisingly, in spite of its wide occurrence and use, there is still a lack of basic physicochemical and biological properties of melatonin. It is the purpose of this work to use recently determined solubilities of melatonin [1–3] to obtain Abraham descriptors, and then to use these descriptors to deduce a large number of physicochemical and biological properties.
2 Methods

We have previously used water–solvent partition coefficients and solubilities of compounds in water and organic solvents to obtain properties or descriptors of compounds [4–9]. The method relies on two general linear free energy relationships, Eqs. 1 and 2, that are used to correlate the transfer of neutral solutes from water to organic solvents and from the gas phase to organic solvents. The dependent variable in Eq. 1 is \( \log_{10} P \), where \( P \) is the molar water to solvent partition coefficient for a series of solutes, and in Eq. 2 it is \( \log_{10} K \) where \( K \) is the dimensionless gas phase to solvent partition coefficient for a series of solutes.

In Eqs. 1 and 2 the independent variables, or descriptors, are properties of the neutral solutes as follows [4–9]. \( E \) is the solute excess molar refraction in \( \text{cm}^3\cdot\text{mol}^{-1}/10 \), \( S \) is the solute dipolarity/polarizability, \( A \) is the overall solute hydrogen bond acidity, \( B \) is the overall solute hydrogen bond basicity, \( V \) is McGowan’s characteristic molecular volume in \( \text{cm}^3\cdot\text{mol}^{-1}/100 \) and \( L \) is the logarithm of the gas to hexadecane partition coefficient at 298 K. Coefficients in Eqs. 1 and 2 are shown in Table 1 for systems that we have used in the current study.

For pure liquid compounds, \( E \) is obtained from the refractive index of the compound at 293 K [4, 5, 9] and for gases and solids the refractive index can be estimated or \( E \) itself can be calculated quite easily [10, 11]. For neutral molecules, the descriptors \( S, A \) and \( B \) can be obtained from water to solvent partition measurements, and from molar solubilities in nonaqueous solvents, \( C_S \) [4–9] The latter can be transformed into water–solvent partition coefficients through Eq. 3, where \( C_W \) is the corresponding molar solubility in water. If \( C_W \) is not known, it can be allowed to ‘float’ and become another descriptor to calculate.

\[
\log_{10} P = c + eE + sS + aA + bB + vV
\]  

\[
\log_{10} K = c + eE + sS + aA + bB + lL
\]  

\[
P = C_S/C_W \quad \log_{10} P = \log_{10} C_S - \log_{10} C_W
\]  

\[
\log_{10} K - \log_{10} K_W = \log_{10} P
\]
Table 1: Coefficients in Eq. 1 and in Eq. 2; calculated (calc) and observed (obs) values of $\log_{10} P$ and $\log_{10} K$ for transfer of melatonin from water and from the gas phase to solvents at 298 K

| Solvent             | c    | e    | s    | a    | b    | l    | v    | Calc   | Obs   |
|---------------------|------|------|------|------|------|------|------|--------|-------|
| Octan-1-ol, wet     | 0.413| 0.077| 0.326| −1.566| −4.391| 0.000| 3.364| log$_{10}$ P | 0.515 | 0.500 |
| Methanol            | 0.276| 0.334| −0.714| 0.243| −3.320| 0.000| 3.549| log$_{10}$ P | 1.086 | 0.949 |
| Ethanol             | 0.222| 0.471| −1.035| 0.326| −3.596| 0.000| 3.857| log$_{10}$ P | 0.714 | 0.687 |
| Propan-1-ol         | 0.139| 0.405| −1.029| 0.247| −3.767| 0.000| 3.986| log$_{10}$ P | 0.460 | 0.488 |
| Butan-1-ol          | 0.165| 0.401| −1.011| 0.056| −3.958| 0.000| 4.044| log$_{10}$ P | 0.179 | 0.299 |
| Pentan-1-ol         | 0.150| 0.536| −1.229| 0.141| −3.864| 0.000| 4.077| log$_{10}$ P | 0.117 | 0.209 |
| Isobutanol          | 0.188| 0.354| −1.127| 0.016| −3.568| 0.000| 3.986| log$_{10}$ P | 0.247 | 0.217 |
| 2-Methoxyethanol    | 0.175| 0.326| −0.140| 0.000| −4.086| 0.000| 3.630| log$_{10}$ P | 1.216 | 1.169 |
| 2-Ethoxyethanol     | 0.133| 0.392| −0.419| 0.125| −4.200| 0.000| 3.888| log$_{10}$ P | 1.022 | 1.054 |
| 1,2-PEG$^a$         | −0.149| 0.754| −0.966| 0.684| −3.134| 0.000| 3.247| log$_{10}$ P | 0.843 | 0.734 |
| Methyl acetate      | 0.351| 0.223| −0.150| −1.035| −4.527| 0.000| 3.972| log$_{10}$ P | 0.229 | 0.113 |
| Ethyl acetate       | 0.328| 0.369| −0.446| −0.700| −4.904| 0.000| 4.150| log$_{10}$ P | −0.177 | −0.086 |
| Propyl acetate      | 0.362| 0.280| −0.390| −0.975| −4.928| 0.000| 4.183| log$_{10}$ P | −0.382 | −0.338 |
| Butyl acetate       | 0.248| 0.356| −0.501| −0.867| −4.973| 0.000| 4.281| log$_{10}$ P | −0.429 | −0.497 |
| Pentyl acetate      | 0.182| 0.216| −0.474| −1.017| −4.952| 0.000| 4.388| log$_{10}$ P | −0.571 | −0.603 |
| IPM$^b$             | −0.605| 0.930| −1.153| −1.682| −4.093| 0.000| 4.249| log$_{10}$ P | −1.560 | −1.486 |
| Gas–water           | −0.994| 0.577| 2.549| 3.813| 4.841| 0.000| −0.869| log$_{10}$ Kw | 15.05 | 15.09 |
| Octan-1-ol, wet     | −0.222| 0.088| 0.701| 3.473| 1.477| 0.851| 0.000| log$_{10}$ K | 15.69 | 15.59 |
| Methanol            | −0.039| −0.338| 1.317| 3.826| 1.396| 0.773| 0.000| log$_{10}$ K | 16.13 | 16.04 |
| Ethanol             | 0.017| −0.232| 0.867| 3.894| 1.192| 0.846| 0.000| log$_{10}$ K | 15.77 | 15.78 |
| Propan-1-ol         | −0.042| −0.246| 0.749| 3.888| 1.076| 0.874| 0.000| log$_{10}$ K | 15.52 | 15.58 |
| Butan-1-ol          | −0.004| −0.285| 0.768| 3.705| 0.879| 0.890| 0.000| log$_{10}$ K | 15.25 | 15.39 |
| Pentan-1-ol         | −0.002| −0.161| 0.535| 3.778| 0.960| 0.900| 0.000| log$_{10}$ K | 15.16 | 15.30 |
| Isobutanol          | −0.003| −0.357| 0.699| 3.595| 1.247| 0.881| 0.000| log$_{10}$ K | 15.29 | 15.31 |
| 2-Methoxyethanol    | −0.141| −0.265| 1.810| 3.641| 0.590| 0.790| 0.000| log$_{10}$ K | 16.23 | 16.27 |
| 2-Ethoxyethanol     | −0.064| −0.257| 1.452| 3.672| 0.662| 0.843| 0.000| log$_{10}$ K | 16.11 | 16.15 |
| Solvent          |  $c$  |  $e$  |  $s$  |  $a$  |  $b$  |  $l$  |  $v$  | Calc $\log_{10} K$ | Obs $\log_{10} K$ |
|------------------|-------|-------|-------|-------|-------|-------|-------|---------------------|------------------|
| 1,2-PEG\(^a\)  | −0.607| 0.239 | 1.008 | 4.278 | 1.755 | 0.706 | 0.000 | 15.98              | 15.83            |
| Methyl acetate   | 0.134 | −0.477| 1.749 | 2.678 | 0.000 | 0.876 | 0.000 | 15.14              | 15.21            |
| Ethyl acetate    | 0.182 | −0.352| 1.316 | 2.891 | 0.000 | 0.916 | 0.000 | 14.92              | 15.01            |
| Propyl acetate   | 0.246 | −0.346| 1.318 | 2.537 | 0.000 | 0.916 | 0.000 | 14.67              | 14.76            |
| Butyl acetate    | 0.147 | −0.414| 1.212 | 2.623 | 0.000 | 0.954 | 0.000 | 14.67              | 14.60            |
| Pentyl acetate   | 0.154 | −0.424| 1.172 | 2.506 | 0.000 | 0.962 | 0.000 | 14.54              | 14.49            |
| IPM\(^b\)        | −0.696| −0.122| 0.575 | 2.027 | 0.777 | 0.999 | 0.000 | 13.76              | 13.61            |
| Gas–water        | −1.271| 0.822 | 2.743 | 3.904 | 4.814 | −0.213| 0.000 | 15.12              | 15.09            |

\(^a\)1,2-Propylene glycol

\(^b\)Isopropyl myristate
where $K_W$ is the dimensionless air to water partition coefficient defined through Eq. 5, where $C_W$ and the corresponding gaseous concentration, $C_G$, are in units of mol·dm$^{-3}$. $K_W$ is the reciprocal of the Henry’s law constant in water, with due regard to units.

$$K_W = C_W / C_G$$

(5)

### 3 Results and Discussion

We have solubilities of melatonin in fifteen different solvents [1–3], and these can then be converted into fifteen partition coefficients through Eq. 3 provided that a numerical value of $\log_{10} C_W$ is known. In instances where $\log_{10} C_W$ and $\log_{10} K_W$ are not available, they can be calculated as part of the regression analysis from measured solubility data for melatonin dissolved in several organic solvents. That will be the case in the current study. The corresponding values of the gas–solvent partition coefficients can then be obtained through Eq. 5. Finally, all the $\log_{10} P$ values yield air–solvent partition coefficients through Eq. 4. We also have a directly determined water–(wet) octanol partition coefficient [12], and two equations in $\log_{10} K_W$, making a total of 34 equations, see Table 1. $E$ was obtained from a calculated refractive index [13], as 1.60 and $V$ was calculated as 1.8251 [3, 10, 11]. We then have the descriptors $S$, $A$, $B$, $L$, $\log_{10} K_W$ and $\log_{10} C_W$ to obtain from a set of 34 simultaneous equations. The set was solved by trial-and-error to yield the descriptors in Table 2 with a standard deviation, $SD$ between observed and back-calculated dependent variables of only 0.084 $\log_{10}$ units. The dependent variables ($\log_{10} P$ or $\log_{10} K$) are listed in Table 1. The calculation procedure is identical to that used in determining the solute descriptors of telmisartan [14], xanthone [15], $o$-acetoacetanisidide [16], 1,3,5-trinitrobenzene [17], caprolactam [7], levetiracetam [18] and other crystalline nonelectrolyte organic compounds. In each of the afore-mentioned instances the numerical values of $\log_{10} C_W$ and $\log_{10} K_W$ were determined as part of the regression analysis.

The descriptors for melatonin are not exceptional. The compound is dipolar ($S=2.46$) as expected from its structure, Fig. 1, and it has quite a large hydrogen-bond acidity ($A=0.95$) due to the amide-NH and the indole-NH hydrogen atoms. Once the descriptors for melatonin have been determined, they can be used in a very large number of equations on the lines of Eq. 1 to calculate partition coefficients from water to some 100 wet solvents, 100 dry solvents and 90 ionic liquids [19]. Then with $\log_{10} C_W = -1.099$, the corresponding solubilities can be obtained through Eq. 3. This seems to be the first time that any general method for calculation of partition coefficients and solubilities of melatonin has been developed.

Because of the use of melatonin supplements, it is of some importance to use our descriptors to calculate biological properties of melatonin. We give in Table 3, coefficients in Eq. 1 for a number of blood–tissue distributions at 313 K [20, 21], and for water–skin partition coefficients and permeability coefficients, again at 313 K [20]. In addition to predicting molar solubilities and blood to tissue distribution coefficients we can calculate the vapor pressure [22], standard molar enthalpies of vaporization [23] and sublimation [24] at 298.15 K, enthalpies of solvation of solvation in 30 different organic solvents [25–29], limiting diffusion coefficients in water and in seven organic

| $E$ | $S$ | $A$ | $B$ | $V$ | $L$ | $\log_{10} K_W$ | $\log_{10} C_W$ |
|-----|-----|-----|-----|-----|-----|----------------|-----------------|
| 1.60 | 2.46 | 0.95 | 1.41 | 1.8251 | 10.189 | 15.09 | $-1.099$ |

### Table 2

Descriptors for melatonin obtained by solution of the set of 34 simultaneous equations

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solvents [30], and the “baseline” median lethal molar concentrations of melatonin towards several aquatic organisms, including six species of fish [31] and three species of water fleas [32] by substituting the numerical values of the solute descriptors given in Table 2 into our previously published Abraham model correlations. For example, we calculate numerical values of $-158 \text{ kJ mol}^{-1}$ and $-132.3 \text{ kJ mol}^{-1}$ for the standard molar enthalpies of solvation of melatonin dissolved in pyridine [27] and dichloromethane [32] at $298.15 \text{ K}$, respectively, and the estimated equilibrium vapor pressure, $VP$, above solid melatonin at $298.15 \text{ K}$ [22] is $VP = 1.8 \times 10^{-18} \text{ atm}$. We were unable to find measured experimental values for melatonin for the fore-mentioned blood to tissue distribution coefficients, aquatic toxicities, and physical and thermodynamic properties in the published literature.

### 4 Conclusions

We have shown that properties, or descriptors, of melatonin can be obtained from molar solubilities in organic solvents. These properties then describe the chemical nature of melatonin, such as dipolarity and hydrogen-bond acidity and basicity. They can be used, together with equations that we have constructed previously, to predict a huge number of physicochemical properties. In view of the use of melatonin supplements, the prediction of biological properties of melatonin is of considerable importance, and this is what we have been able to do.

### Declarations

**Conflict of interest** There are no conflicts of interest to declare.
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