Low Noise Frequency-Domain Multiplexing of TES Bolometers Using SQUIDs at Sub-Kelvin Temperature

T. Elleflot1 · A. Suzuki1 · K. Arnold2 · C. Bebek1 · R. H. Cantor3 · K. T. Crowley4 · J. Groh5 · T. de Haan6 · A. Hornsby4 · J. Joseph1 · A. T. Lee1,4 · T. Liu7 · J. Montgomery8 · M. Russell2 · Q. Yu4

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Abstract
Digital Frequency-Domain Multiplexing (DfMux) is a technique that uses MHz superconducting resonators and Superconducting Quantum Interference Device (SQUID) arrays to read out sets of transition edge sensors. DfMux has been used by several Cosmic Microwave Background experiments, including most recently POLARBEAR-2 and SPT-3 G with multiplexing factors as high as 68, and is the baseline readout technology for the planned satellite mission LiteBIRD. Here, we present recent work focused on improving DfMux readout noise, reducing parasitic impedance, and improving sensor operation. We have achieved a substantial reduction in stray impedance by integrating the sensors, resonators, and SQUID array onto a single-carrier board operated at 250 mK. This also drastically simplifies the packaging of the cryogenic components and leads to better-controlled crosstalk. We demonstrate a low readout noise level of 8.6 pA/Hz$^{1/2}$, which was made possible by operating the SQUID array at a reduced temperature and with a low dynamic impedance. This is a factor of two improvement compared to the achieved readout noise level in currently operating Cosmic Microwave Background experiments using DfMux and represents a critical step toward maturation of the technology for the next generation of instruments.

Keywords Frequency-domain multiplexing · Transition edge sensors · Readout electronics · Cosmic Microwave Background
1 Introduction

Digital Frequency-Domain Multiplexing (DfMux) [1–3] is a TES multiplexing technique, in which sets of ∼1 Ω TES bolometers are placed in series with superconducting LC resonators [4] that define unique $\mathcal{O}(1)$ MHz bias frequencies. A voltage bias is applied to each detector at the resonance frequency of its associated LC resonator, and the resulting current is actively nulled. Residual current is amplified by a cryogenic DC SQUID array and room temperature electronics and used to rapidly update the nulling current [5]. DfMux has been deployed in many Cosmic Microwave Background (CMB) experiments, including most recently POLARBEAR-2 and SPT-3G with multiplexing factors as high as 68 [6]. DfMux is also the baseline readout technology for the planned CMB satellite mission LiteBIRD [7].

Here, we present recent work aimed at reducing readout noise and parasitic impedance and improving readout packaging [8, 9]. In section 2, we describe the hardware used for these measurements, including a technology demonstrator circuit board called the Cold Integrated Multiplexing Module (CIMM). The CIMM moves all cryogenic readout components onto a single circuit board that is cooled to 250 mK, reducing parasitic impedances that generate crosstalk and detector instability [1, 10, 11] and simplifying the readout packaging. In section 3, we present results from measurements performed using the CIMM, which include a factor of two reduction in readout noise and factor of five reduction in parasitic resistance compared to currently operating CMB DfMux systems. We conclude in Section 4.

2 Implementation

This work was done using a technology demonstrator circuit board called the CIMM, described previously in [8]. In contrast with deployed DfMux systems, in which the cryogenic readout components are spread across two cryogenic temperature stages [12], the CIMM holds all cryogenic readout components on a single printed circuit board at 250 mK. This dramatically reduces the parasitic impedance associated with the electrical connection between the SQUID and resonators, which is a source of crosstalk [1, 11], and relaxes the requirements on the $\mathcal{O}(1)$m cable that spans the 4 K to 250 mK temperature differential, allowing us to use commercial twisted pair cable instead of the custom low-inductance cables used in deployed instruments.

Due to a subtlety of the SQUID feedback scheme used, the inductance of the SQUID array input coil and parasitic series inductance provide a mechanism for bias frequency-dependent readout noise [6, 11]. We designed the CIMM such that only on-chip impedances contribute to this effect (see Fig. 1). We chose to use an SA13ax SQUID array because of its low input inductance of 70 nH [13], high transimpedance, and variable dynamic impedance. The SA13ax is also used in the SPT-3G and PB-2 receivers at a temperature of 4 K.

The CIMM also holds one LC resonator chip and up to five TES chips, allowing us to operate 40 detectors. The TES bias is provided by a 4.2-nH controlled
The use of a reactive bias element reduces power dissipation on the sub-kelvin stage and provides a small reduction in readout noise. The use of a reactive TES bias element has been studied previously, e.g., \[1, 8, 10, 14\].

Magnetic shielding was provided by several layers of high magnetic permeability foil (Metglas 2705 M). Care was taken to ensure that no ferromagnetic materials were used in the fabrication of the circuit board. The assembly was installed on the sub-kelvin stage of a cryostat cooled with a pulse tube cryocooler and a helium adsorption cooler with a base temperature of 250 mK. The connection from the CIMM to the room temperature electronics is made with twisted pair cable.

### 3 Results

#### 3.1 SQUID Performance

We measured flux modulation curves at several temperatures between 4 K and 250 mK. The modulation curves were smooth at 4 m, but irregularities were observed on the rising slope of the curve at temperatures of 800 mK and below. The irregularities limit our choice of bias point and are thought to be associated with excess SQUID noise. Others have demonstrated reduced SQUID noise by using an RC snubber in parallel with the SQUID input coil [15]. We found that shunting the input coil with a 5 \(\Omega\) cryogenic resistor completely removed the irregularities at all accessible temperatures (see Fig. 2). The resistor and input inductance of the SQUID input coil form a low-pass filter. We chose the shunt resistance value such that the cutoff frequency of the filter is above our readout bandwidth. During CIMM operation, the shunt resistor is at a temperature of 250 mK and its Johnson noise makes a negligible contribution to the total readout noise.

SQUID tuning is the process by which a current and flux bias are applied to the SQUID in order to achieve an optimum between readout noise and SQUID linearity.
Tuning is usually performed using an automated routine, but can also be performed manually. After tuning, the transimpedance ($Z_t$) and dynamic impedance ($R_{dyn}$) of the array at the chosen bias point, defined below, can be measured [13, 16].

\begin{align}
Z_t &= \frac{\partial V}{\partial \Phi} M_{in} \\
R_{dyn} &= \left( \frac{\partial I_{SQ}}{\partial \Phi} \right)^{-1}
\end{align}

In the equations above, $V$ is the voltage across the SQUID, $\Phi$ is the magnetic flux applied to the SQUID, $I_{SQ}$ is the SQUID bias current, and $M_{in}$ is the mutual inductance of the SQUID and input coil.

We performed the automated SQUID tuning routine at several temperatures between 4 K and 250 mK and found that $Z_t$ and $R_{dyn}$ increased by 60% and 20%, respectively, over this temperature range. We also investigated the achievable range of $Z_t$ and $R_{dyn}$ values by manually tuning the SQUID to eleven different bias points while holding the CIMM at a constant temperature of 250 mK (Fig. 3). We observe a correlation between $Z_t$ and $R_{dyn}$, which should be expected due to the common factor of $\frac{\partial V}{\partial \Phi}$ in their definitions. Using manual tuning, it is possible to increase $Z_t$ by nearly a factor of two relative to the automated routine.

### 3.2 Readout Noise

Power absorbed by a bolometer is transduced into an amplitude modulation of the SQUID feedback current associated with the bolometer’s bias frequency [5]. In the absence of signals and detector noise, we can take the demodulated signal as a measurement of readout noise. To perform this measurement, we replaced the TES sensors with 1 $\Omega$ resistors, which do not have a superconducting transition in the relevant temperature range and do not have sensitivity to optical power. The resistors
contribute Johnson noise to the measurement, which we conservatively estimated by assuming a low electron temperature of 250 mK and a resistance of 1 Ω. This is removed when analyzing readout noise data, though it only accounts for about 10% of the total measured noise.

The SQUID dynamic impedance impacts readout noise in two ways: It converts the input current noise of the first-stage amplifier into a voltage noise at the output of the SQUID, and it forms a low-pass filter with the capacitance of the cryogenic wiring between the SQUID and 300 K amplifier [11]. For the SA13ax, \( \frac{\partial I_{\text{sq}}}{\partial \phi} \) can take significantly different values on the positive and negative slopes of the modulation curve, resulting in \( R_{\text{dyn}} \) of \( \sim 300 \Omega \) (\( \sim 700 \Omega \)) on the positive (negative) slope while maintaining a constant \( Z_t \sim 1000 \Omega \). This allowed us to measure the impact of \( R_{\text{dyn}} \) on readout noise. We found that operating the SQUID with low \( R_{\text{dyn}} \) resulted in a reduction in readout noise of 6–8 pA/Hz\(^{1/2}\) across the range of bias frequencies compared to operating with high \( R_{\text{dyn}} \). This is consistent with our expectations based on the current noise of the room temperature amplifier. The latter effect was not expected to be important for this measurement because we are using a short length of cryogenic wiring with low-pass cutoff frequencies well above our readout bandwidth for both values of \( R_{\text{dyn}} \), and indeed the invocation of this effect is not required to explain the measured readout noise.

Next, we studied the effect of SQUID tuning on readout noise (Fig. 3). We measured readout noise, while the CIMM was cooled to 250 mK for eleven different manual SQUID tunings. Despite the change in \( Z_t \) and \( R_{\text{dyn}} \) by a factor of about two over the range of current biases, we measure only a \( \sim 10\% \) change in median readout noise. We previously described a correlation between \( R_{\text{dyn}} \) and readout noise, and this measurement implies an anti-correlation between \( Z_t \) and readout noise. Together, these observations are consistent with the dominant noise.

![Fig. 3](Color figure online) Measured values of \( Z_t \) and \( R_{\text{dyn}} \) (top) and readout noise (bottom) at 250 mK with several different values of current bias applied to the SQUID array.
source being the first-stage amplifier following the SQUID. The broad minimum in readout noise indicates that there is flexibility in optimizing SQUID linearity without significantly affecting readout noise performance. The lowest achieved median noise level is \(8.6 \text{ pA/Hz}^{1/2}\). This represents a factor of two reductions in readout noise compared to currently observing CMB experiments using DfMux. The bias frequency dependence of the readout noise is also greatly suppressed (Fig. 4). We measure an increase in noise by about 15% at our highest bias frequencies, which should be compared to a \(\sim 100\%\) increase in noise in deployed CMB DfMux systems.

We refer the measured readout noise to the input of a LiteBIRD-like bolometer by assuming a 1 \(\Omega\) TES operating resistance and a conservative 1 pW electrical bias power [17]. In all observing bands, the measured readout noise is below the projected LiteBIRD sensitivity [18].

### 3.3 TES Operation

We verified TES operation by simultaneously lowering the voltage biases applied to a set of TES bolometers such that they cooled through their superconducting transitions. This was done by first heating the CIMM above the critical temperature of the sensors (\(\sim 450\) mK) and applying a large voltage bias of \(\sim 10\) \(\mu\)V using the CIMM’s inductive bias element. We then cooled the CIMM to its base temperature and then incrementally decreased the voltage biases while measuring the resulting current. The results are shown in Fig. 5. A total of 30 bolometers were electrically connected, and we successfully operated 28. There are broad stable regions on many channels. Several channels become unstable at high fractional resistance, and we suspect that this is due to a mismatch between the detector and electrical bandwidths, rather than instability due to parasitic impedance. The residual resistance measured after the detector is superconducting [10, 19] contributes to crosstalk and detector instability at low operating resistance. The measured values have a median of 60 m\(\Omega\), which is a reduction by about a factor of five compared to currently deployed systems.

![Fig. 4](image.png) Measured readout noise as a function of bias frequency for 36 channels. The median value is \(8.6 \text{ pA/Hz}^{1/2}\). The slight increase in noise with frequency is likely due to an effect related to the SQUID feedback [6] and is suppressed significantly compared to deployed instruments.
4 Conclusions

We have demonstrated several improvements to TES multiplexing using DfMux readout, including a substantial reduction in readout noise and operation of many TES bolometers under an inductive bias. The reduction in readout noise is a crucial step toward future applications of DfMux readout. The noise reduction was achieved by operating the SQUID array at lower temperature and with low dynamic impedance tuning. Additionally, parasitic impedances which are known to affect the frequency dependence on the readout noise have been significantly reduced by the circuit board design. The decrease in residual superconducting resistance in the TES bias circuit will allow for TES operation at lower resistance, resulting in higher responsivity and a further suppression of readout noise compared to deployed CMB DfMux systems. The improvements made to the cryogenic architecture significantly relax the constraints on the cryogenic cables, making the cryogenic packaging more robust and much simpler to procure. We are developing a version of the CMM that is compatible with the POLARBEAR-2 receivers, and we hope to deploy several CIMM modules in the near future. The datasets generated during and/or analyzed during the current study are available from the corresponding author on reasonable request.

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Authors and Affiliations

T. Elleflot\textsuperscript{1} \(\ast\) \cdot A. Suzuki\textsuperscript{1} \cdot K. Arnold\textsuperscript{2} \cdot C. Bebek\textsuperscript{1} \cdot R. H. Cantor\textsuperscript{3} \cdot K. T. Crowley\textsuperscript{4} \cdot J. Groh\textsuperscript{5} \cdot T. de Haan\textsuperscript{6} \cdot A. Hornsby\textsuperscript{4} \cdot J. Joseph\textsuperscript{1} \cdot A. T. Lee\textsuperscript{1,4} \cdot T. Liu\textsuperscript{7} \cdot J. Montgomery\textsuperscript{8} \cdot M. Russell\textsuperscript{2} \cdot Q. Yu\textsuperscript{4}

\textsuperscript{1} Lawrence Berkeley National Laboratory, Physics Division, Berkeley, CA 94720, USA
\textsuperscript{2} Department of Physics, University of California San Diego, San Diego, CA 92093, USA
\textsuperscript{3} STAR Cryoelectronics, Santa Fe, NM 87508, USA
\textsuperscript{4} Department of Physics, University of California Berkeley, Berkeley, CA 94720, USA
\textsuperscript{5} National Institute of Standards and Technology, Boulder, CO 80305, USA
\textsuperscript{6} High Energy Accelerator Research Organization (KEK), Tsukuba, Ibaraki 305-0801, Japan
\textsuperscript{7} Electrical and Computer Engineering Department, Princeton University, Princeton, NJ 08540, USA
\textsuperscript{8} Physics Department, McGill University, Montreal, QC H3A 0G4, Canada