GOLDRUSH. III. A Systematic Search of Protoclusters at $z \sim 4$ Based on the $> 100\,\text{deg}^2$ Area

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Abstract

We conduct a systematic search for galaxy protoclusters at $z \sim 3.8$ based on the latest internal data release (S16A) of the Hyper SuprimeCam Subaru Strategic program (HSC-SSP). In the Wide layer of the HSC-SSP, we investigate the large-scale projected sky distribution of $g$-dropout galaxies over an area of $121\,\text{deg}^2$, and identify $216$ large-scale overdense regions ($> 4\sigma$ overdensity significance) that are good protocluster candidates. Of these, $37$ are located within $8\,\text{arcmin}$ ($3.4\,\text{physical Mpc}$) from other protocluster candidates of higher overdensity, and are expected to merge into a single massive structure by $z = 0$. Therefore, we find $179$ unique protocluster candidates in our survey. A cosmological simulation that includes projection effects predicts that more than $76\%$ of these candidates will evolve into galaxy clusters with halo masses of at least $10^{14}\,M_\odot$ by $z = 0$. The unprecedented size of our protocluster candidate...
1 INTRODUCTION

Structure formation in the universe proceeds hierarchically. Small perturbations in the initial density field grow and merge together over time, leading to the emergence of a cosmic web: a filamentary structure with voids and overdensities (Bertschinger 1998). How galaxy clusters, the largest overdensities at the nodes of this web, are assembled remains an open question. In which respect does the evolution of galaxies residing in these highest density peaks differ from that of those in the field? To address this question, it is necessary to directly investigate all the evolutionary stages of galaxy clusters through cosmic time, including their progenitors, “protoclusters” (Overzier 2016). In the local universe, galaxy clusters exhibit tight red sequences, composed of massive quiescent galaxies, and can be traced by X-ray emission from the hot gas trapped in their massive dark matter halos. Increasing redshifts, the fraction of star-forming galaxies becomes higher, and quiescent galaxies would be a rare galaxy population even in overdense environments at $z \gtrsim 2$. Galaxies in protoclusters are predicted to be the first to transition from star-forming to quiescent due to environmental effects. Numerical simulations suggest that at early epochs these galaxies may experience enhanced accretion and galaxy merger rates (Somerville & Davé 2015). Protoclusters thus represent a unique laboratory for the study of early (massive) galaxy growth. However, direct empirical data in support of these expectations remains elusive. Despite their importance, protoclusters remain poorly understood due to their rarity. So far, the number of known protoclusters in the early universe ($z \gtrsim 3$) is limited to less than a dozen systems (e.g., Venemans et al. 2007; Toshikawa et al. 2016).

To find such rare protoclusters at high redshifts, radio galaxies (RGs) and quasars (QSOs) are commonly used as tracers of protoclusters (e.g., Wylezalek et al. 2013; Adams et al. 2015) because these galaxies hosting powerful active galactic nuclei (AGN) are thought to be embedded in massive dark matter halos. However, not all RGs and QSOs appear to reside in high-density environments (Hatch et al. 2011; Mazzucchelli et al. 2017; Uchiyama et al. 2017), and Hatch et al. (2014) found that although RGs are found in environments that are, on average, relatively biased compared to other galaxies, they can be found in a wide range of low- to high-density environments based on a study of 419 RGs. It is therefore still unclear if, and how the AGN activity in, for example, RGs and QSOs is related to their surrounding environments. Because of non-uniformity AGN duty cycles, we also expect that a large fraction of protoclusters would be missed if using powerful AGNs as tracers. Furthermore, strong radiation from RGs and QSOs could also result in a suppression of galaxy formation (e.g., Barkana & Loeb 1999; Kashikawa et al. 2007). Therefore, in order to avoid possible selection biases, it has been a longstanding goal to search for protoclusters in large “blank” field. At $z \sim 1–2$, many galaxy clusters have been discovered by blank surveys (e.g., Rettura et al. 2014). Beyond $z \sim 3$, while some protoclusters that do not host RGs or QSOs have been discovered (Steidel et al. 1998; Ouchi et al. 2005), the number of such protoclusters is still very small due to very limited sky coverage at a sufficient depth. Based on a relatively wide $4\,\text{deg}^2$ optical imaging survey of the Canada-France-Hawaii Telescope Legacy Survey Deep Fields and follow-up spectroscopy, the number density of protoclusters was found to be only $\sim 1.5\,\text{deg}^{-2}$ at $z \sim 4$ (Toshikawa et al. 2016).

Here, we present a systematic survey of protoclusters at $z \sim 3.8$ based on the wide-field survey with the Hyper SuprimeCam (HSC: Miyazaki et al. 2012) conducted as part of the Subaru strategic program (SSP). The HSC is mounted at the prime focus of the Subaru telescope and has a large field-of-view (FoV) of $1.8\,\text{deg}^2$. The wide-field imaging capability of the HSC enables us to find high-redshift protoclusters in large blank fields with relative ease. The HSC-SSP started in early 2014 and will be completed by 2019. The HSC-SSP is composed of three layers, the UltraDeep (UD; $3.5\,\text{deg}^2$, $i \sim 28\,\text{mag}$), the Deep ($26\,\text{deg}^2$, $i \sim 27\,\text{mag}$), and the Wide layers ($1400\,\text{deg}^2$, $i \sim 26\,\text{mag}$) (Aihara et al. 2017). By using the extremely wide-area coverage and the high sensitivity through five op-
tical broad-bands (g-, r-, i-, z-, and y-bands), we construct a systematically selected sample of protoclusters at $z \gtrsim 3$. The present paper is one in the series of papers on Lyman break galaxies (LBGs) based on the HSC-SSP, named Great Optically Luminous Dropout Research Using Subaru HSC (GOLDRUSH), which include sample selection and UV luminosity function (Ono et al. 2017), clustering analysis (Harikane et al. 2017), and protocluster search presented in this paper. In addition, Uchiyama et al. (2017) and Onoue et al. (2017) discuss the relation between LBG overdensity and QSOs by using the sample of protocluster candidates constructed in this paper. The HSC-SSP also allows us to study high-redshift Lyα emitters (LAEs) by narrow-band imaging as the project of Systematic Identification of LAEs for Visible Exploration and Reionization Research Using Subaru HSC (SILVERRUSH: Ouchi et al. 2017; Shibuya et al. 2017a, 2017b; Konno et al. 2017). This paper is organized as follows. Section 2 describes the selection of $z \sim 3.8$ galaxies and the systematic sample of protocluster candidates. In Section 3, we investigate the spatial distribution of protocluster candidates through a clustering analysis. We will discuss the dark matter halo mass of protoclusters based on a systematic sample of protocluster candidates in Section 4. The summary is given in Section 5. We assume the following cosmological parameters: $\Omega_m = 0.3$, $\Omega_{\Lambda} = 0.7$, $H_0 = 100h \text{ km s}^{-1} \text{ Mpc}^{-1} = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, and magnitudes are given in the AB system.

2 PROTOCLUSTER CANDIDATES

2.1 Selection of $z \sim 3.8$ Galaxies

In this paper, we make use of the latest internal HSC-SSP data release (S16A). The current UD and Deep layers have not yet reached the final depths of the five-year HSC-SSP. In the Wide layer, the survey area at full depth has been steadily increasing as the HSC-SSP proceeds. The sky coverage with all five broad-bands (g, r, i, z, and y) is 178 $\text{deg}^2$ in the Wide layer of the S16A data release, and already dozens of times larger than any previous survey capable of detecting protoclusters at $z \gtrsim 3$. Therefore, in this paper, we focus on a systematic search for protoclusters at $z \sim 3.8$ in the Wide layer as our initial attempt. Although the Wide layer is composed of three large regions (two around the spring and autumn equator and the other around the Hectmap region) at the end, the current Wide data release includes six disjoint regions in the XMM-LSS, GAMA09H, WIDE12H, GAMA15H, HECTOMAP, and VVDS fields.

Image reduction, object detection, and photometry were performed by the reduction pipeline of the HSC-SSP (hsPipe; see the details in Bosch et al. (2017)). From this HSC-SSP catalog in the Wide layer, we select $z \sim 3.8$ galaxy candidates using the Lyman break technique ($g$-dropout galaxies). The construction of dropout galaxies is described in Ono et al. (2017), and this study of protocluster search is constructed based on this catalog though we apply some modifications on the sample selection in order to meet our requirements. We use the following color-selection criteria (van der Burg et al. 2010; Toshikawa et al. 2016), which are the same with those of Ono et al. (2017):

$$1.0 < (g-r) < 1.0 \land 1.5(r-i) < (g-r) - 0.80.$$  

In order to accurately estimate their color, we only use objects detected at more than 5$\sigma$ and 3$\sigma$ significance in the $i$- and $r$-bands, respectively; a 3$\sigma$ limiting magnitude for the $g$-band was used in the $g-r$ color if objects were fainter than the 3$\sigma$ limiting magnitude in the $g$-band. We use the CModel magnitude, which is determined by fitting two-component, PSF-convolved galaxy models (de Vaucouleurs and exponential), to estimate color. For point sources, the CModel magnitude is consistent with a PSF magnitude. Our color criteria are sensitive to galaxies in the redshift range of $z \sim 3.3\sim 4.2$, corresponding to $\Delta z \sim 740 \text{ comoving Mpc}$. The locus of contaminants (e.g., dwarf stars and passive galaxies at $z \sim 0.5$) lies far from the selection region on the two-color diagram composed of $g-r$ and $r-i$ (Toshikawa et al. 2016). In addition to these color criteria, we remove objects which are located at the edge of images, cosmic rays, saturated, and bad pixels by using the flags flags_pixel_edge, flags_pixel_interpolated_center, flags_pixel_saturation, flags_pixel_cr_center, flags_pixel_bad, which are products of hscPipe indicating the reliability of the measurements. Objects near bright stars are also masked by means of the flags flags_pixel_bright_object_center and flags_pixel_bright_object any. It should be noted that the mask used around bright stars is very large ($\gtrsim 1 \text{ deg}$ diameter) for very bright stars in the current version of the HSC-SSP catalog. From these criteria of colors, detection significances, and measurement flags, nearly one million of $g$-dropout galaxies are obtained in all six regions of the Wide layer, with number counts that are consistent with those of van der Burg et al. (2010) (see Ono et al. (2017) for detail).

2.2 Identification of Protocluster Candidates

The depth in the Wide layer is inhomogeneous over the whole area because the sky conditions vary during the long-term observations; furthermore, even in the same portion of the Wide layer, all five optical filters are not observed in the same night. The inhomogeneity of depth could make a large impact on the number of detected objects, making it difficult to fairly compare number density among different fields. The hscPipe processes HSC imaging data separately in 1.7 $\times$ 1.7 $\text{deg}^2$ rectangular tracts, and a tract is further divided into sub-regions of 12 $\times$ 12 $\text{arcmin}^2$ patches. We estimate the sky noise of each patch, determined as the standard deviation of sky flux measured by the PSF photometry (Figure 1). We search for proto-
which will coalesce into a single massive halo of this radius. This radius is expected to be the typical extent of regions (2016), which is by counting the number of quantified by following the same method as in Toshikawa et al. regions within an aperture of ∆z ≤ 0.03) is tens times smaller than the redshift range of g-dropout galaxies. It is possible that an alignment of two small structures by chance shows significantly high density, while the overdensity of protoclusters can diminish due to fore/background void regions. The apertures are distributed over the Wide layer in a grid pattern with intervals of 1 arcmin. By using only apertures in which the masked area is less than 5%, the mean and the dispersion, σ, of the number of g-dropout galaxies in an aperture are found to be 6.4 and 3.2, respectively. The difference of the mean among the five fields of the Wide layer is only 0.54 (0.17σ) at most. Thus, while the limiting magnitudes of each field are slightly different, it is confirmed that we obtain a highly uniform sample over all five regions by limiting the selection to g-dropout galaxies to be brighter than 25.0 mag and removing patches in which the g-, r-, and i-band depths are shallower than our criteria. Both statistical errors and cosmic variance should contribute to the estimate of σ (Somerville et al. 2004), but the derived σ is almost equal to that expected from Poisson statistics (Gehrels 1986) due to the small number of g-dropout galaxies in an aperture. The detailed study of cosmic variance at high redshift will be addressed based on the HSC-Deep layer. In this study, we only aim to identify significantly overdense regions rather than to accurately map environments from low to high density. The surface number density of g-dropout galaxies in masked regions is assumed to be the same as the mean, but apertures in which > 50% area is masked are excluded in our protocluster search. Overdensity is defined as the excess surface number density from the mean, and overdensity contours of the Wide layer are plotted in Figure 2.

Since the central ∼ 1 deg² area of the UD-COSMOS overlaps with the Canada-France-Hawaii Telescope Legacy Survey (CFHTLS) Deep 2 field, we can make a consistency check of our overdensity estimate by directly comparing with the overdensity contours of g-dropout galaxies in the CFHTLS (Toshikawa et al. 2016). The same color selection of g-dropout galaxies and overdensity estimate described above are applied
Fig. 2. Overdensity contours of $g$-dropout galaxies. Higher density regions are indicated by redder colors. The white regions are regions that are masked due to survey edges, bright stars, or insufficient depth. The positions of the unique 179 protocluster candidates are indicated by red circles. The area of all panels are shown at the same scale.
to both the HSC and CFHTLS dataset. As shown in Figure 3, the overdensity contours derived by the HSC dataset are clearly consistent with that of the CFHTLS dataset, suggesting that we can correctly map overdensity in the Wide layer as well.

The distribution of overdensity significance in the Wide layer largely deviates from the expected distribution from the Poisson distribution at the high-overdensity end (Figure 4). For example, the number of $4\sigma$ overdense regions is $\sim 30$ times higher than the expectation from Poisson distribution. Thus, high overdense regions would be resulted from clustering of physically associated galaxies rather than chance alignment due to projection effect. Furthermore, we have also compared with a theoretical prediction derived from the light-cone model of Henriques et al. (2012) by selecting mock $g$-dropout galaxies and applying the same overdensity measurements (see §3.2 in Toshikawa et al. (2016) for details). The observed distribution is consistent with that of the model prediction, although the model somewhat underestimates the number of $> 6\sigma$ overdensity significance regions. Such overdense regions are extremely rare, and the excess observed in the Wide layer over the simulations comes as no surprise given that the volume of our survey is $\sim 1$ Gpc$^3$ compared to the volume of $\sim 0.4$ Gpc$^3$ for the simulation from which the light-cone models are extracted. The model thus reasonably reproduces the observed overdensity distribution except at the extreme high-density end, and the mass of descendant halo at $z = 0$ can be deduced from the halo merger trees given by the simulation. As shown in Chiang et al. (2013) and Toshikawa et al. (2016), the surface overdensities observed toward protoclusters are statistically correlated with the descendant halo mass at $z = 0$ though we expect a large scatter caused by the redshift uncertainty of the dropout galaxies (see §3.2 in Toshikawa et al. (2016) for details). Protocluster candidates are defined as regions where the overdensity significance is $> 4\sigma$ at the peak. With this definition, 76% of these candidates are expected to evolve into galaxy clusters of $> 10^{14} M_\odot$ at $z = 0$, and the overdensities of the others are enhanced by projection effects though they will be smaller structures than galaxy clusters. On the contrary, only $\sim 6\%$ of progenitors of $> 10^{14} M_\odot$ halos at $z = 0$ are expected to be located on $> 4\sigma$ regions at $z \sim 4$ because the overdensity of most of progenitors are decreased by the projection effects. Our selection method for protocluster candidates can make a clean sample with high purity, though its completeness is small. It should be noted that our sample has low contamination, guaranteeing minimal effects of contamination on our measurements of angular clustering (Section 3). Because our selection strategy minimises the selection of structures suffering from large projection effects, our sample of protocluster candidates will be biased to the richest structures with the average descendant halo mass of $\sim 5 \times 10^{13} M_\odot$.

We have found 216 $> 4\sigma$ overdense regions of $g$-dropout galaxies in the Wide layer. The individual overdense regions show a wide range of morphologies (Figure 5). The morphology of these overdense regions will eventually provide clues to understand galaxy/halo assembly from the large-scale structure of the universe, but this is beyond the scope of this paper. Some overdense regions have neighboring overdense regions within a few arcmin (Figure 5). Although, as mentioned above, 0.75 physical Mpc (1.8 arcmin) is the typical extent of protoclusters, protocluster galaxies can be located a few or more physical Mpc away from their centers depending on the direction of filamentary structure (e.g., Muldrew et al. 2015). It is unlikely that two overdense regions are located within a few arcmin just by chance because the mean separa-
Fig. 5. Examples of the protocluster candidates. The points indicate g-dropout galaxies. Individual protocluster candidates exhibit unique shapes, and some are accompanied by several other overdense regions (e.g., bottom-left and top-right panels).

Fig. 6. Observed angular correlation function of all protocluster candidates. The solid and dashed lines show the best-fitted power laws in the case of fixed and free β, respectively.

tion is ~ 40 arcmin based on the surface number density of overdense regions. Toshikawa et al. (2016) quantitatively investigated how far protocluster members are typically spread from the center and found that galaxies lying within the volume of $R_{sky} < 8(6)$ arcmin and $R_e < 0.013(0.010)$ at $z \sim 3.8$ will be members of the same protocluster with a probability of $> 50(80)\%$. Overdense regions which are located near each other are expected to merge into a single structure by $z = 0$. In this study, if $> 4\sigma$ overdense regions are located within 8 arcmin from another more overdense region, they can be regarded as the substructures of that protocluster though spectroscopic follow-up will be required to distinguish from chance alignment. Of 216 > 4σ overdense regions, 37 have neighboring more overdense regions. The fraction of neighboring overdense regions is significantly higher than that expected by uniform random distribution ($N = 10.6 \pm 3.2$), implying that the large fraction of neighboring overdense regions are physically associated with each other rather than chance alignment. As a result, we have found 216 protocluster candidates at $z \sim 3.8$, and 179 of them would trace the unique progenitors of galaxy clusters in the Wide layer, which is about ten times larger than any previous study of protoclusters ($N \sim 10–20$ at $z \gtrsim 3$). According to Toshikawa et al. (2016), three out of four protocluster candidates identified by the same method are confirmed to be real protoclusters by spectroscopic follow-up observations, which is consistent with the model prediction.

3 ANGULAR CLUSTERING

Based on the systematic sample produced by the HSC-SSP, we investigate the spatial distribution of protocluster candidates at $z \sim 3.8$ through the angular correlation function, $\omega(\theta)$. In order to include any small-scale structure in the correlation function, in this analysis we use all > 4σ overdense regions instead of only unique protocluster candidates. We measure the observed $\omega(\theta)$ using the estimator presented in Landy & Szalay (1993):

$$\omega_{\text{obs}}(\theta) = \frac{DD(\theta) - 2DR(\theta) + RR(\theta)}{RR(\theta)}$$

where DD, DR, and RR are the number of unique data-data, data-random, and random-random pairs with angular separation between $\theta - \Delta \theta/2$ and $\theta + \Delta \theta/2$, respectively. As shown in Figure 5, the overdense regions are generally found to have 3–6 arcmin extents within $\gtrsim 2\sigma$ regions and show various, complex shapes. The coordinate of overdense regions is simply defined as the position of their overdensity peak. The locations of surface overdensity peaks can be affected by projection effects, but the typical uncertainty is expected to be only 0.5 arcmin ($\sim 2$ arcmin at worst) by using theoretical models (Toshikawa et al. 2016). We distribute 40,000 random points in the same geometry as protocluster candidates. The uncertainty of $\omega_{\text{obs}}(\theta)$ is estimated using the bootstrap method as follows. We randomly select our protocluster candidates, allowing for redundancy, and calculate $\omega_{\text{obs}}(\theta)$. This calculation is repeated 100 times, and the uncertainty of each angular bins is determined by the root mean square of all of the bootstrap steps. Figure 6 shows the angular correlation function for all > 4σ overdense regions at $z \sim 3.8$ in the Wide layer.

The angular correlation function can be parameterized by a power law: $\omega(\theta) = A_\omega \theta^{-\beta}$. The slope, β, is found to be $\sim 1.0$, which does not strongly depend on redshift and mass of clusters at $z \lesssim 2$ (e.g., Bahcall et al. 2003; Papovich 2008). We use a least-square technique to fit a power-law function to the angular
correlation function. The observed angular correlation function is biased to lower amplitude because the size of the survey field is finite. Thus, the true angular correlation function is estimated by adding a constant value, known as the integral constraint:

$$\omega(\theta) = \omega_{obs}(\theta) + \frac{\sum A_\omega \theta^{-\beta} RR(\theta)}{\Sigma RR(\theta)} + \frac{1}{N},$$

(2)

where $N$ is the number of objects. Since the angular correlation function, $\omega(\theta)$, is the projected three-dimensional spatial correlation function, $\xi(\theta)$, we can derive $\xi(\theta)$ from $\omega(\theta)$ if the redshift distribution of protocluster candidates is known (Limber 1953; Phillipps et al. 1978). The spatial correlation function can also be parameterized by a power law of $\xi(r) = (r/r_0)^{-\gamma}$. The slope, $\gamma$, is related to $\beta$ as $\gamma = \beta + 1$, and the correlation length, $r_0$, is estimated from the following equation:

$$r_0 = \left( \frac{A_\omega}{H_\gamma} \right) \left( \frac{\int f(z) dN_{\gamma} d\xi}{\int f(z) dN_{\gamma} d\xi} \right)^{1/\gamma},$$

(3)

where $f(z)$ describes the redshift dependence of $\xi(r)$, $dN_{\gamma}$ is the comoving distance, $dN/dz$ is the redshift selection function, $E(z)$ and $H_\gamma$ are defined as:

$$E(z) = \frac{H_0}{c} \left[ \Omega_m (1+z)^3 + \Omega_\Lambda \right]^{1/2},$$

(4)

$$H_\gamma = \sqrt{\frac{\Gamma(\gamma-1/2)}{\Gamma(\gamma/2)}}.$$

(5)

We use $f(z) = [(1+z)/(1+z_c)]^{-(3+\epsilon)}$, where $z_c$ is the typical redshift of protocluster candidates and $\epsilon = 1.2$ (Roche & Eales 1999). Solving Equation 3, we assume that the redshift selection function of protocluster candidates corresponds to that of $g$-dropout galaxies. The redshift selection function is derived by the same method as in Toshikawa et al. 2016). In the case $\beta$ is fixed to 1.0, we derive $r_0 = 35.0^{+0.9}_{-0.8} h^{-1}$ Mpc. When both $\beta$ and $r_0$ are free parameters, the best-fitted values are found to be $\beta = 1.34 \pm 0.20$ and $r_0 = 35.7^{+1.6}_{-0.8} h^{-1}$ Mpc. Although there is a slight difference in the value of $\beta$, the $r_0$ derived in the case of fixed $\beta$ corresponds to that in the case of free $\beta$ within 1$\sigma$ uncertainty. It should be noted that we assume that the redshift distribution of protocluster is identical to that of $g$-dropout galaxies, though it is unlikely that protoclusters are found at the lower- or higher-ends of the redshift selection function of $g$-dropout galaxies; thus, the redshift distribution of protoclusters may be narrower. If there are systematical differences of physical properties between protocluster and field galaxies, their redshift tracks on two-color diagram and redshift distribution could also be different. So far, significant differences between protocluster and field galaxies have not been found at $z \gtrsim 4$ though only a few protoclusters have been investigated to date (Overzier et al. 2009). To evaluate the redshift distribution of protoclusters is beyond this study, and further detailed studies are required (e.g., systematic follow-up spectroscopy, or model comparison).

4 HALO MASS ESTIMATE

The mass of dark matter halo is one of key quantities to characterize the physical properties of protoclusters because the evolution of dark matter halo or the formation of the large-scale structure are relatively well-understood compared with complex baryon physics. Once the dark matter halo mass is estimated at high redshifts, we can predict the descendant halo mass in the context of hierarchical structure formation model. However, in actual observations, protocluster candidates are defined by the number density of galaxies, and it is not straightforward to estimate their halo mass. For local clusters, velocity dispersion is frequently used to measure halo mass, and the same technique applies to protoclusters at high redshifts; however, protoclusters would be far from virialization. Another method is based on galaxy number density, which can be converted into mass density by using the bias parameter; then, mass can be calculated by the volume of a protocluster (e.g., Steidel et al. 1998; Venemans et al. 2007). It should be noted that the mass estimated by this way means total mass which will collapse into a single structure rather than current halo mass at high redshift.

In this study, we show two alternative approaches. The one is abundance matching by assuming protoclusters occupy all most massive dark matter halos, and the other is to utilize the clustering strength of protocluster candidates estimated in Section 3. We use these method on protocluster candidates at $z \sim 3.8$ for the first time because a systematic sample is required.

4.1 Abundance Matching

The number density of the protocluster candidates is estimated to be $n = 4.6 \times 10^{-7} h^3$ Mpc$^{-3}$ by assuming that the redshift selection function of protoclusters is identical to that of $g$-dropout galaxies. The number density of protocluster candidates is found to correspond to that of dark matter halos of $\sim 0.8 - 1.1 \times 10^{13} h^{-1} M_\odot$ at $z \sim 3.8$ (Figure 7). The difference of cosmology or mass function model does not have a large effect on the estimate of halo mass. In the same manner, it would be possible to predict the descendant halo mass at $z = 0$, though we need to consider the change of the number density from $z \sim 3.8$. If individual protocluster candidates will evolve different clusters, or the number density at $z = 0$ is identical to that at $z \sim 3.8$, the descendant halo mass of protocluster candidates is expected to be $\sim 6.3 \times 10^{14} h^{-1} M_\odot$. However, as discussed in Section 2.2, some protocluster candidates have other neighboring protocluster candidates. Since such protocluster candidates can merge into single massive structures, the number density at $z = 0$ will be smaller than at $z \sim 3.8$. In case that protocluster candidates located within the half of mean separation (20 arcmin) will coalesce into a single halo by $z = 0$, the number density is decreased by 37%. Along with the decline of number density, the expected descendant halo mass is increased.
to \( \sim 7.6 \times 10^{14} h^{-1} M_\odot \). As shown in Figure 7, the slope of mass function is very steep at the high-mass end; hence, the estimate of halo mass based on abundance matching have a small dependence on the fraction of protocluster merging.

4.2 Clustering

We also calculated the dark matter halo mass of our protocluster candidates based on our clustering analysis. We have used the analytical model proposed by Sheth et al. (2001) and Mo \\& White (2002), which has been shown to provide a connection between the bias of the dark matter halo and the mass of the dark matter halo based upon ellipsoidal collapse (Sheth et al. 2001), provided the bias of the dark matter halo and the redshift are given. We estimate the mean dark matter halo mass, \( \langle M_h \rangle \), from a comparison between the effective bias parameter and the bias of the dark matter halo. The dark matter halo mass was estimated as \( \langle M_h \rangle = 2.3^{+0.5}_{-0.3} \times 10^{13} h^{-1} M_\odot \), which is roughly consistent with that estimated by the abundance matching. According to this dark matter halo mass at \( z \sim 3.8 \), the descendant halo mass at \( z = 0 \) is evaluated as \( \langle M_h \rangle = 4.1^{+0.7}_{-0.5} \times 10^{14} h^{-1} M_\odot \) using the extended Press-Schechter model.

4.3 Relation between Abundance and Clustering Strength

Next, we investigate the relation between the spatial number density, \( n \), and the correlation length of protocluster candidates. Younger et al. (2005) found that the \( n-r_0 \) relation does not vary with redshift based on \( N \)-body dark matter simulations. The consistency in the \( n-r_0 \) relation across redshift can be explained as resulting from the fact that galaxy clusters occupy the high-mass end of the halo mass function. The formation of such massive structure started in the early universe, and the abundance of galaxy clusters or their progenitors at high redshift does not dramatically vary with redshifts. The correlation length of galaxy clusters is furthermore relatively stable assuming that they do not move very far away from their initial location. Younger et al. (2005) proposed an analytic approximation to the \( \Lambda \)CDM \( n-r_0 \) relation of

\[
   r_0 = 1.7 \left( \frac{n}{h^3 \text{Mpc}^{-3}} \right)^{-0.2} h^{-1} \text{Mpc}. \tag{6}
\]

According to Equation 6, the correlation length is calculated to be \( r_0 = 31.4 h^{-1} \text{Mpc} \) from the number density, which is consistent with the one derived from the clustering analysis (Figure 8). The values of \( r_0 \) and \( n \) found for our sample of protocluster candidates are comparable to those of X-ray-selected galaxy clusters (e.g., Bahcall et al. 2003). The correlation length is larger than that of optically-selected local clusters (Postman et al. 1992) and Spitzer selected clusters at \( z \sim 1 \) (Papovich 2008), but very similar to that of mid-infrared selected clusters at \( z \sim 1.5 \) in the South Pole Telescope Deep Field survey (Rettura et al. 2014). This result suggests that our protocluster candidates are tracing very similar spatial structures as those ex-
pected of the progenitors of rich clusters and enhances the confidence that our method to identify protoclusters at high redshifts is robust.

5 SUMMARY

We have presented a systematic sample of protoclusters at \( z \sim 3.8 \) in the HSC-Wide layer based on the latest internal data release of the HSC-SSP (S16A). The unprecedentedly wide survey of the HSC-SSP allowed us to perform a large protocluster search without having to rely on preselection of common protocluster probes (e.g., RGs or QSOs). We selected a total of 216 overdense regions with an overdensity significance greater than \( 4\sigma \). Of these, 37 can be considered to be substructures of a larger overdensity region, and thus in total we have identified 179 unique protocluster candidates. By comparing with theoretical models, we found that \( > 76\% \) of them are expected to evolve into galaxy clusters of \( > 10^{14} M_\odot \) by \( z = 0 \). We investigated for the first time the spatial distribution of protoclusters through clustering analysis, and the correlation length is found to be \( r_0 = 34.1 \, h^{-1} \) Mpc. Both the abundance matching method and the clustering analysis resulted in consistent protocluster halo masses of \( \sim 1 - 2 \times 10^{13} M_\odot \) at \( z \sim 3.8 \). These halos are expected to evolve into galaxy clusters of \( \geq 5 \times 10^{14} M_\odot \) by \( z = 0 \) (Figures 7 and 8). The relation between number density and correlation length is consistent with the prediction of the \( \Lambda \)CDM model, suggesting that our sample of protocluster candidates at \( z \sim 3.8 \) indeed probes the progenitors of local rich clusters. When the HSC-SSP is completed, we expect that > 1000 protoclusters will be identified at \( z \sim 3.8 \) from the Wide layer and a total of \( \sim 100 \) protoclusters from \( z \sim 2 \) to \( z \sim 6 \) will be found from the UD and Deep layers. Based on the systematic sample of protoclusters across cosmic time, we will be able to understand the process of cluster formation from their birth to maturity.

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