Observations of a doubly driven V system probed to a fourth level in laser-cooled rubidium

S. R. de Echaniz, Andrew D. Greentree, A. V. Durrant, D. M. Segal, J. P. Marangos and J. A. Vaccaro

1Quantum Processes Group, Department of Physics and Astronomy, The Open University, Walton Hall, Milton Keynes, MK7 6AA, UK
2Laser Optics and Spectroscopy Group, Blackett Laboratory, Imperial College of Science, Technology and Medicine, London SW7 2BZ, UK
3Department of Physics and Astronomy, University of Hertfordshire, Hatfield AL10 9AB, UK

(October 24, 2018)

Observations of a doubly driven V system probed to a fourth level in an N configuration are reported. A dressed state analysis is also presented. The expected three-peak spectrum is explored in a cold rubidium sample in a magneto-optic trap. Good agreement is found between the dressed state theory and the experimental spectra once light shifts and uncoupled absorptions in the rubidium system are taken into account.

42.50.Hz, 32.80.-t, 42.50.Gy, 42.62.Fi

I. INTRODUCTION

The optical properties of coherently prepared atoms have been much studied in recent years. The simplest case is when one transition is resonantly pumped with a strong coherent laser beam and the resulting dressed system probed from a third level in a Λ, V or cascade configuration. These systems can exhibit electromagnetically-induced transparency (EIT) where quantum interference effects allow a resonant probe beam to propagate without absorption and with greatly-enhanced dispersion. The EIT effect has been exploited in a variety of applications: gain without inversion, ground state cooling of trapped atoms, ultra-slow light-speed propagation, quantum non-demolition measurements and efficient non-linear optical processes. This has lead to interest in more complex systems involving multiple electromagnetic fields interacting with either a single transition or with several transitions. In particular there is now huge interest in exploiting non-linearities in four-level systems with applications in quantum optics and four-wave mixing.

Four-level systems of various configurations can be excited with different pumping schemes. Several theoretical studies have considered three-level ladder configurations coherently prepared by two strong laser beams. They predict a three-peak spectrum when the lowest or highest of the three levels is probed via a fourth level or monitored by fluorescence. When the two dressing beams are on resonance this spectrum has the form of a Doppler-free three-photon absorption peak situated centrally within an EIT window. More generally, the positions and intensities of the three peaks are functions of the Rabi frequencies and detunings of the two strong beams. The trajectories of the peaks as a function of Rabi frequencies and detunings have been described in doubly dressed analyses. None of these three studies was accompanied by experimental verifications.

In this paper we consider a similar scheme to those of references but with the two strong pump beams, or coupling beams as we shall call them, connecting a ground or metastable level to two excited levels. The resulting dressed V system can then be probed from another ground or metastable level, as illustrated in Figure 1(a). An experimental realisation in 87Rb cooled in a magneto-optic trap (MOT) is indicated in Figure 1(b). Our interest in this system stems from our current programme of work on the strong cross- and self-phase modulation expected in the N-configuration of Figure 1, and the main aim of this paper is to characterise the weak-probe spectrum of this system. For this task we have to be concerned not only with the behaviour of the ideal four-level model (Figure 1(a)) but also with light shifts due to off-resonant interactions with other nearby hyperfine levels and the effects of level degeneracies in the 87Rb system. Because our experiments are carried out in a Rb MOT, we are free to propagate our beams in any desired directions, and to choose coupling beams on different optical transitions that are well-separated in frequency thus avoiding potentially complex mutual light shifts induced by the two beams, although some simple light shifts and the effects of the trapping beams do have to be taken into account in the system of Figure 1(a).

Many manifestations of Zeeman degeneracy have been reported in EIT experiments: optical pumping among Zeeman levels and to other levels, coherent population trapping by the coupling beam, the inversion of EIT dips (i.e. electromagnetically induced absorption), and absorption of the probe beam on Zeeman transitions that are not coupled by the pump beam. These latter uncoupled absorptions are a constant feature of our probe spectra, superimposed on the V system spectra we are interested in.

This paper is organised as follows. Section II presents a dressed state analysis of the strongly-pumped model V system of Figure 1(a), showing the expected depen-
dence of the probe absorption spectrum on Rabi frequencies and detunings. Section III describes the experimental arrangement and presents EIT spectra with the first coupling field $C_1$ applied and the second coupling field $C_2$ switched off, thus showing the effects of light shifts and uncoupled absorptions in a relatively simple system. Our main results are presented in Section IV where both coupling fields are applied and probe spectra obtained for various coupling field intensities and detunings. The spectra are interpreted using the 4-state theory of Section II modified phenomenologically by the light shift and uncoupled absorption effects described in Section III. We justify the use of the four-state model and we describe the origin of the uncoupled absorptions relevant to our experiments in the Appendix.

II. THEORY

Figure 1(a) shows a four state N configuration, although for the purposes of this discussion we shall consider it as a three state V scheme formed by the states $|a\rangle$, $|c\rangle$ and $|d\rangle$ and strong coupling fields $C_1$ and $C_2$ of frequencies $\omega_1$ and $\omega_2$, probed weakly on the $|b\rangle-|d\rangle$ transition. The Hamiltonian describing the system consisting of the atom and the two coupling fields can be written down in the semiclassical and rotating wave approximations as

$$\mathcal{H} = \mathcal{A} + \mathcal{I}$$

where

$$\mathcal{A} = \Delta_1 |a\rangle \langle a| + (\Delta_1 - \Delta_2) |c\rangle \langle c|$$

$$\mathcal{I} = \frac{\Omega_1}{2} (|d\rangle \langle a| + |a\rangle \langle d|) + \frac{\Omega_2}{2} (|c\rangle \langle a| + |a\rangle \langle c|).$$

$\mathcal{A}$ and $\mathcal{I}$ represent the atomic and interaction parts of the Hamiltonian $\mathcal{H}$. $\Delta_1 = \omega_1 - \omega_{da}$ ($\Delta_2 = \omega_2 - \omega_{ca}$) is the detuning of coupling field $C_1$ ($C_2$) from the $|a\rangle - |d\rangle$ ($|a\rangle - |c\rangle$) transition and $\omega_{j\alpha}$ is the transition frequency of the $|\alpha\rangle - |\beta\rangle$ transition for $\alpha, \beta = a, b, c, d$. $\Omega_j = d_j \cdot E_j$ is the Rabi frequency for field $j = 1, 2$ where the field $E_j$ interacts only with its quasi-resonant transition with electric dipole moment $d_j$. We have chosen units such that $\hbar = 1$ so energies are measured in units of frequency.

Because there are three basis states which describe the system, in the most general case, we expect a characteristic three line spectrum when performing probe absorption experiments. Writing out the Hamiltonian in matrix form gives

$$\mathcal{H} = \begin{bmatrix} \Delta_1 & \Omega_2/2 & \Omega_1/2 \\ \Omega_2/2 & \Delta_1 - \Delta_2 & 0 \\ \Omega_1/2 & 0 & 0 \end{bmatrix}.$$  \hspace{1cm} (1)

Following the method in Shore [17] we derive the doubly dressed state energies

$$\mathcal{E}_1 = -\frac{1}{3} \alpha + \frac{2}{3} \rho \cos \left(\frac{\Theta}{3}\right)$$

$$\mathcal{E}_2 = -\frac{1}{3} \alpha - \frac{2}{3} \rho \cos \left(\frac{\Theta}{3} + \frac{\pi}{3}\right)$$

$$\mathcal{E}_3 = -\frac{1}{3} \alpha - \frac{2}{3} \rho \cos \left(\frac{\Theta}{3} - \frac{\pi}{3}\right)$$

with
\[
\begin{align*}
\alpha &= -2\Delta_1 + \Delta_2 \\
\beta &= \Delta_1(\Delta_1 - \Delta_2) - \frac{1}{4}(\Omega_1^2 + \Omega_2^2) \\
\gamma &= \frac{1}{4}(\Delta_1\Omega_1^2 - \Delta_2\Omega_2^2) \\
p &= \sqrt{\alpha^2 - 3\beta} \\
\cos \Theta &= \frac{-27\gamma + 2\alpha^2 - 9\alpha\beta}{2p^3}.
\end{align*}
\]

The corresponding dressed state vector for energy \(\mathcal{E}_\nu\) is

\[
|D_\nu\rangle = \frac{1}{\mathcal{N}_\nu} \left( |\nu\rangle |a\rangle + (\mathcal{E}_\nu (\mathcal{E}_\nu - \Delta_1) - \frac{\Omega_1^2}{4}) |c\rangle + \frac{\Omega_1\Omega_2}{4} |d\rangle \right)
\]

with

\[
\mathcal{N}_\nu = \sqrt{\epsilon_\nu^2 \Omega_2^2 + (\mathcal{E}_\nu (\mathcal{E}_\nu - \Delta_1) - \frac{\Omega_1^2}{4})^2 + \frac{\Omega_1^2 \Omega_2^2}{16}}
\]

being the normalisation constant and \(\nu = 1, 2, 3\) indexing the dressed state.

We now consider the special case of mutual resonance of the two coupling fields, i.e. \(\Delta_1 = \Delta_2 = 0\). In this case the dressed state energies and vectors are

\[
\begin{align*}
\mathcal{E}_1 &= \frac{1}{2}\sqrt{\Omega_1^2 + \Omega_2^2} \\
\mathcal{E}_2 &= 0 \\
\mathcal{E}_3 &= -\frac{1}{2}\sqrt{\Omega_1^2 + \Omega_2^2}
\end{align*}
\]

and

\[
\begin{align*}
|D_1\rangle &= \frac{1}{\sqrt{2}} \left( |a\rangle + \frac{\Omega_2}{\sqrt{\Omega_1^2 + \Omega_2^2}} |c\rangle + \frac{\Omega_1}{\sqrt{\Omega_1^2 + \Omega_2^2}} |d\rangle \right) \\
|D_2\rangle &= 0 |a\rangle - \frac{\Omega_1}{\sqrt{\Omega_1^2 + \Omega_2^2}} |c\rangle + \frac{\Omega_2}{\sqrt{\Omega_1^2 + \Omega_2^2}} |d\rangle \\
|D_3\rangle &= \frac{1}{\sqrt{2}} \left( -|a\rangle + \frac{\Omega_2}{\sqrt{\Omega_1^2 + \Omega_2^2}} |c\rangle + \frac{\Omega_1}{\sqrt{\Omega_1^2 + \Omega_2^2}} |d\rangle \right).
\end{align*}
\]

These results can be used to predict the spectrum obtained when probing the doubly driven \(|c\rangle - |d\rangle\) transition via the \(|b\rangle - |d\rangle\) transition with a weak field of frequency \(\omega_p\) and detuning \(\Delta_p = \omega_p - \omega_{db}\). The resulting spectrum can be thought of as being made up of a Rabi split doublet, with effective Rabi frequency \(\Omega_{\text{eff}} = \sqrt{\Omega_1^2 + \Omega_2^2}\), and a three-photon resonance absorption peak at \(\Delta_p = 0\).

The central peak is strictly only on the three-photon resonance (i.e. satisfies \(\Delta_p - \Delta_1 + \Delta_2 = 0\)) when \(\Delta_1 = \Delta_2\), or in appropriate limits. However, for simplicity we shall refer to the central peak as a three-photon absorption peak when it closely approximates this resonance condition. We note that the probe coupling will be dominated by the \(|b\rangle - |d\rangle\) transition as the other transitions are significantly off resonance in the bare atomic basis. Also, in the strong coupling regime \((\Omega_1, \Omega_2 \gg \Omega_p)\), which applies in our experiments, almost all the population is optically pumped into the state \(|b\rangle\) with negligible population in the dressed states. Under these conditions the probe absorption will be proportional to the coefficient \(A_\nu = |\langle d |D_\nu\rangle|^2\). This implies that the peaks corresponding to the absorption from state \(|b\rangle\) to the outer states \(|D_1\rangle\) and \(|D_3\rangle\) will have equal heights and dominate the spectrum in the limit \(\Omega_2/\Omega_1 \gg 1\), whilst the three-photon absorption peak, corresponding to absorption to \(|D_2\rangle\), will dominate in the limit \(\Omega_2/\Omega_1 \gg 1\). Graphs showing the energy levels \(\mathcal{E}_\nu\) and coefficients \(A_\nu\) as a function of \(\Omega_2/\Omega_1\) are presented in Figures 2(a) and (b) respectively. These results are similar to those presented for a ladder system by Wei et al. [10]
FIG. 3. Schematic of the experimental arrangement showing beam polarisations. Field \( C_1 \) is linearly polarised in the vertical plane whilst fields \( C_2 \) and \( P \) are linearly polarised in the horizontal plane. The angle between fields \( C_1 \) and \( C_2 \) is about 175\(^\circ\), whilst the angle between \( C_1 \) and \( P \) is about 20\(^\circ\). \( PD \) is an avalanche photodiode. The trapping fields are not shown for clarity.

III. EXPERIMENTAL ARRANGEMENT, LIGHT SHIFTS AND EIT EFFECTS

The experimental setup is shown schematically in Figure 3. The cold \(^{87}\)Rb sample contains between \( 10^7 \) and \( 10^8 \) atoms in a region of diameter approximately 3 mm in a standard MOT similar to the one used in our previous work on EIT [13].

The laser fields are obtained from external-cavity grating-controlled diode lasers (ECDL) in master and master-slave arrangements. The frequency of each master laser is monitored by saturated absorption in a room temperature Rb cell and can be locked via electronic feedback. In all master-slave arrangements, there is an acousto-optic modulator which shifts the frequency of the slave relative to the frequency of the master. All laser fields, except for the second coupling field, were derived from 780 nm laser diodes, whilst the second coupling field was derived from a 795 nm laser diode.

The trapping lasers \( T \) (not shown in Figure 3) are derived from a master-slave system. They are locked and detuned by \(-13\) MHz from the \( 5S_{1/2}F = 2 \) to \( 5P_{3/2}F = 3 \) transition. The trapping beam diameters are \( \approx 1 \) cm and the total average intensity in the cold atom sample is \( \approx 60 \) mW/cm\(^2\).

The probe beam \( P \) is derived from an ECDL and is scanned across the \( 5S_{1/2}F = 2 \) to \( 5P_{3/2}F = 2 \) transition by piezo-control of the external cavity. \( P \) has an average intensity \( \approx 2 \) mW/cm\(^2\) in a diameter \( \approx 1 \) mm.

The coupling beam \( C_1 \) and the trap repumping field \( R \) are derived from the same laser which is the slave of a locked ECDL. They are resonant with the \( 5S_{1/2}F = 1 \) to \( 5P_{3/2}F = 2 \) transition. The average intensity of \( C_1 \) is \( \approx 400 \) mW/cm\(^2\) in a roughly elliptical profile 2 mm \( \times \) 4 mm.

A second coupling beam \( C_2 \) is derived from an ECDL and is quasi-resonant with the \( 5S_{1/2}F = 1 \) to \( 5P_{1/2}F = 2 \) transition at 795 nm (the D\(_1\) line). For resonant experiments, \( C_2 \) was locked, but for detuned experiments it was stepped using the external cavity piezo with the frequency determined by an optical spectrum analyser. The average intensity of \( C_2 \) can be varied up to a maximum of \( \approx 300 \) mW/cm\(^2\), in a beam diameter \( \approx 1.3 \) mm.

The probe \( P \) and the second coupling field \( C_2 \) are linearly polarised in the horizontal plane whilst the coupling field \( C_1 \) is linearly polarised in the vertical direction. The angle between the coupling fields \( C_1 \) and \( C_2 \) is about 175\(^\circ\) while the probe propagates at an angle of about 20\(^\circ\) with respect to \( C_1 \). These angles were found to give a good overlap of the probe with the coupling fields in the MOT. The paths of all three beams are coplanar.

We show in the Appendix how our arrangement of polarisations gives a good approximation to three separate sets of \( N \) configurations of the type depicted in Figure 1(a), together with uncoupled absorption. Although we can qualitatively account for the uncoupled absorptions, the relative populations of the various subsystems will be affected by the trap dynamics and optical pumping between the schemes. Complete modelling of these effects is beyond the scope of this work and we have therefore not presented a quantitative theoretical estimate of the uncoupled absorption strength.

While \( C_2 \) is turned off, \( C_1 \) and \( P \) form a \( \Lambda \)-type EIT system. Figure 4(a) shows the probe absorption versus probe detuning with \( C_1 \) locked to the \( 5S_{1/2}F = 1 \) to \( 5P_{1/2}F = 2 \) transition in the saturated absorption cell, and with \( C_2 \) turned off. The probe detuning is taken to be zero when the probe frequency is equal to the \( 5S_{1/2}F = 2 \) to \( 5P_{3/2}F = 2 \) transition frequency in the saturated absorption cell. It is seen that the spectrum consists of a central peak situated between the two Autler-Townes peaks of a standard asymmetric EIT profile expected with detuned coupling field. The detuning of \( C_1 \) is due to the fact that the \( 5S_{1/2}F = 1 \) level of the sample is light-shifted with respect to the same level in the saturated absorption cell because of the interaction of \( C_1 \) with neighbouring transitions (mainly the \( 5S_{1/2}F = 1 \) to \( 5P_{3/2}F = 1 \) transition). We have estimated this light shift to be \( \Delta \approx 7 \) MHz. The central peak in the spectrum is caused by \( P \) probing Zeeman sublevels that are not coupled by \( C_1 \) (as discussed in the Appendix). We call this peak the uncoupled absorption peak; in our previous work [13] we were unable to resolve this peak since the coupling field was too weak. It is to be noted that all three peaks in Figure 4(a) are displaced by approximately 9 MHz with respect to the saturated absorption transition. This is because the trapping beams \( T \) act as a detuned coupling field with \( P \) in a \( \Lambda \)-type EIT configuration, as can be seen from Figure 1(b). This splits each of the three peaks into two, one of which is very much larger than the other because \( T \) is detuned by \(-13\) MHz. Of the smaller peaks, only the one corresponding to the red detuned Autler-Townes peak is just visible in this trace. We note that the linewidths of our spectra, which are seen to be up to three times the natural linewidth of our Doppler-free sample, are broadened by beam profile inhomogeneities, variations of Clebsch-Gordan coefficients between different Zeeman transitions and the spread in the intensities of the six interfering trapping beams in the MOT.
IV. THREE PEAK SPECTRA OF THE V SYSTEM

We now describe the spectra obtained when probing the V system in the N configuration of Figure 1. The probe absorption spectrum shown in Figure 4(b) was obtained with $C_1$ and $C_2$ tuned to their respective transitions in saturated absorption cells; these are the same conditions that applied in Figure 4(a) except that now $C_2$ is switched on and at its maximum intensity. A comparison of the two figures shows that the height $h_c$ of the central peak is larger in Figure 4(b) due to the appearance of the three-photon absorption peak on top of the uncoupled absorption peak, as predicted in the Section II. There is also an increase in the splitting, $\delta_{13} = E_1 - E_3$, of the two Autler-Townes peaks. We have taken a series of probe spectra for different powers $P_2$ of $C_2$. The results are shown in Figures 5(a)&(b), where the height $h_c$ and the splitting $\delta_{13}$ are plotted against the power $P_2$. The theoretical fits in these figures were obtained from the theory in Section II, as follows. We assume that the contribution of the three-photon absorption peak is proportional to $A_2 = |\langle d|D_2 \rangle|^2$, and that both coupling fields have a common detuning of $\Delta = 7$ MHz from their respective transitions in the sample due to the $C_1$-induced light shift of the $5S_{1/2}F = 1$ level. We find, to first order in $\Delta$,

$$\delta_{13} = \sqrt{\Omega_1^2 + \Omega_2^2 + O(\Delta)^2}$$

$$h_c = h_{uc} + B \frac{\Omega_2^2}{\Omega_1^2 + \Omega_2^2} + O(\Delta)^3$$

where $h_{uc}$ is the height of the uncoupled absorption peak, i.e., the height of the central peak when $C_2$ is turned off, and $B$ is a constant. These equations have been fitted to the data points and the resulting curves shown in Figure 5(a)&(b). The fit in Figure 5(a) gives $\Omega_1 = 62 \pm 2$ MHz and $\Omega_2 = (22 \pm 2$ MHz / mW$^{1/2}$)$P_2^{1/2}$ with a maximum of
FIG. 6. Probe spectra showing the migration of the three-peak structure as the detuning $\Delta_2$ of the coupling field $C_2$ is stepped from the red to the blue side of the resonance. The peaks are labelled 1, 2 and 3 corresponding to absorption to levels $E_1$, $E_2$ and $E_3$. The uncoupled absorption peak is labelled U. Each spectrum is an average over 200 scans. 

$\Omega_2 = 44 \pm 5$ MHz. These Rabi frequencies are consistent with the values estimated from the parameters of beams $C_1$ and $C_2$ and the Clebsch-Gordan coefficients of the transitions. The fit in Figure 5(b) gives $\Omega_2/\Omega_1 = 0.8 \pm 0.3$ for maximum $\Omega_2$, which is consistent with the previous fit; it also yields the constant $B = 3 \pm 1$ that determines the relative heights of the uncoupled absorption peak and the three-photon absorption peak. We note that for maximum power of $C_2$ the three-photon absorption peak accounts for approximately 0.4 of the total central peak height.

We now consider the case where $C_2$ has its maximum intensity and its detuning is stepped across the $5S_{1/2}F = 1$ to $5P_{1/2}F = 2$ transition, with $C_1$ tuned to the saturated absorption line. The detuning of $C_2$ is measured by a calibrated spectrum analyser with respect to the saturated absorption line. The traces obtained are plotted in Figure 6. It is seen that as $\Delta_2$ is stepped from the red towards the blue, the uncoupled absorption peak, labelled U, remains fixed in position as expected, but the peaks labelled 1, 2 and 3 migrate towards the red, with the central peak 2 moving across the uncoupled absorption. The positions of peaks 1, 2 and 3 are shown as points in Figure 7 with the curves showing the corresponding theoretical expectations based on a detuning $\Delta_1 = 7$ MHz of $C_1$. We note that this behaviour is qualitatively similar to that predicted for a ladder system in [10]. We note also that the anticrossings in Figure 7 are similar to subharmonic resonances described in [7], although because the two coupling fields are applied to different transitions, only the first subharmonic resonances (at $\Delta_2 = \pm \Omega_1/2$ in the limit of small $\Omega_2$) are observed in the present study.

V. CONCLUSIONS

We have presented a dressed state analysis and an experimental study of a doubly-driven V-system probed from a fourth level in an N configuration. The experiments show the growth of the three-photon absorption peak and the increasing separation of the Autler-Towns peaks as the second coupling field intensity is increased. The migration of the three-peak probe absorption spectrum as the detuning of one of the coupling fields is changed is also observed. Our experiments have been
carried out in a laser-cooled $^{87}$Rb sample using the levels $5P_{3/2} = 2$, $5S_{1/2} = 1$ and $5P_{1/2} = 2$, probed on the $5S_{1/2} = 2$ to $5P_{3/2} = 2$ transition. After taking account of light shifts, the effects of the trapping beams and the uncoupled absorptions in this real system, the measured spectra are in good agreement with the analytical predictions. This investigation is important for the understanding of a physically realisable N-system that might be used in cross-phase modulation, photon blockade and other related studies.

VI. ACKNOWLEDGMENTS

We would like to thank the EPSRC for financial support on this project and Dr T. B. Smith (Open University) for useful discussions. We would also like to thank Roger Bence, Fraser Robertson and Robert Seaton (Open University) for technical assistance.

VII. APPENDIX

This Appendix justifies our use in Section II of a 4-state model to describe our experiment and also shows the origin of the uncoupled absorptions. Figure 8(a) illustrates the individual Zeeman states of the hyperfine levels coupled by the probe $P$ (fine lines) and two driving fields $C_1$ (thick lines) and $C_2$ (double lines) [19]. All three fields are linearly polarised with the polarisation of $C_1$ orthogonal to the polarisations of $P$ and $C_2$ as shown in Figure 3. This particular choice of orthogonal linear polarisations was chosen because it reduced the uncoupled absorption of the probe field at the frequency of the $5S_{1/2} = 2$ to $5P_{3/2} = 2$ transition. Also shown are the corresponding Clebsch-Gordan coefficients. The states $|m\rangle_X$ are labeled in terms of the magnetic quantum number $m$ and $X$, where $X$ is one of $a$, $b$, $c$ or $d$ which correspond to the $5S_{1/2} = 1$, $5S_{1/2} = 2$, $5P_{1/2} = 2$ and $5P_{3/2} = 2$ levels respectively in Figure 1(b).

The figure shows that the coupling field $C_1$ (thick lines) alone provides a doubly-driven $V$ configuration as well as a separate quadruply-driven ‘W’ configuration. Taking account of the additional states coupled by the fields $C_2$ and $P$ it appears that a six state and, separately, a nine state model are necessary to describe the dynamics of our experiment. The three states, $|0\rangle_b$, $|-2\rangle_c$ and $|2\rangle_c$ do not interact with any fields. Surprisingly, however, this complex structure reduces to sets of simple coupled systems with the following change of basis [20]:

\[
|m, \pm\rangle_X \equiv \frac{1}{\sqrt{2}} (|m\rangle_X \pm |-m\rangle_X)
\]

\[
|\alpha\rangle_d \equiv \frac{1}{2} |0\rangle_d + \frac{\sqrt{3}}{2} |2, +\rangle_d
\]

\[
|\beta\rangle_d \equiv \frac{\sqrt{3}}{2} |0\rangle_d - \frac{1}{2} |2, +\rangle_d.
\]

FIG. 8. Zeeman states, coupled transitions and Clebsch-Gordan coefficients in the (a) angular-momentum basis and (b) the new basis. Three separate N configurations are clearly visible in the new basis.

Figure 8(b) shows the transitions in this new basis. Three doubly-driven V configurations, of the type shown in Figure 1(a), are clearly evident in the new basis. Also shown are the effective Clebsch-Gordan coefficients for the new transformed transitions. The dashed lines in Figure 8(b) represent transitions probed by field $P$ but not directly coupled by either of the coupling fields $C_1$ and $C_2$. They correspond to what we call uncoupled absorptions of the probe.

The five coupled states on the left of Figure 8(b) shows that the (relatively weak) field $P$ simultaneously probes a doubly-driven $V$ configuration as well as the $|2, -\rangle_d$ to $|\beta\rangle_d$ transition. In the steady state, the $|2, -\rangle_d$ to $|\beta\rangle_d$ transition simply causes additional scattering of field $P$ and so essentially this five-state system can be treated as a four-state N configuration with an additional uncoupled absorption. The underlying probe absorption profile is due essentially to three separate N configurations (solid lines) with two uncoupled absorptions (dashed lines).

Each N configuration has a different set of (effective) Clebsch-Gordan coefficients, and so the Rabi frequencies for the fields $P$, $C_1$ and $C_2$ differ from one N configuration to the next. Since the position of the peaks in the probe absorption spectrum depend on the Rabi frequencies $C_1$ and $C_2$, the absorption peaks due to each N configuration occur at different probe detunings. However, these differences are relatively small, corresponding
to about a 10% shift in the separation of Autler-Townes peaks. A single four-state model, as given in Section II, is therefore sufficient to model our experiment, provided we allow for broadened absorption peaks.

The square of Clebsch-Gordan coefficients of the dashed transitions is $\frac{1}{6}$. We can compare this with the different scheme in which all fields are linear polarised along the same axis. In this case there are two uncoupled absorption transitions from $|\pm 2\rangle_b$ to $|\pm 2\rangle_d$ for which the square of the corresponding Clebsch-Gordan coefficients is $\frac{2}{3}$. That is, the absorption of the uncoupled transitions in the parallel-linear polarisation scheme is four times that of the orthogonal-linear polarisation scheme for the same degree of occupation. This clearly shows the advantage of our choice of polarisation scheme.

In our experiment, new atoms are continuously moving into and out of the interaction region, the trapping magnetic fields produce Zeeman mixing amongst ground states and the trapping field weakly couples the $5S_{1/2}F = 2$ level to the upper $5P_{3/2}F = 3$ level. All these effects tend to redistribute population amongst the states of the $5S_{1/2}F = 2$ level. The treatment of these effects to calculate the relative occupations of the $5S_{1/2}F = 2$ states is, however, beyond the scope of this work. Thus, while we can identify the transitions responsible for the uncoupled absorptions and justify our polarisation scheme, we have no quantitative estimates of the strength of the absorptions.

Finally we note that state $|0\rangle_b$, uncoupled by any field, is a dark state. Away from resonance conditions that produce other dark states, all atoms would eventually decay to this state and so the steady state would be one of complete transparency of the probe field. However, the above mechanisms which tend to redistribute the population of the $5S_{1/2}F = 2$ level will also tend to depopulate the state $|0\rangle_b$.

[1] J.P. Marangos, J. Mod. Opt., 45, 471-503 (1998); M. Xiao, Y-Q. Li, S-Z. Jin and J. Gea-Banacloche, Phys. Rev. Lett., 74, 666-669 (1995).
[2] O. Kocharovskaya, Phys. Rep. 219, 175 (1992); M.O. Scully, Phys. Rep. 219, 191 (1992).
[3] C. F. Roos, D. Leibfried, A. Mundt, F. Schmidt-Kaler, J. Eschner and R. Blatt, Phys. Rev. Lett. 85, 5547 (2000); G. Morigi, J. Eschner, and C. Keitel, Phys. Rev. Lett. 85, 4458 (2000).
[4] M.M. Kash, V.A. Sautenkov, A.S. Zibrov, L. Hollberg, G.R. Welch, M.D. Lukin, Y. Rostovtsev, E.S. Fry and M.O. Scully, Phys. Rev. Lett., 82, 5229-5231 (1999); L.V. Hau, S.E. Harris, Z. Dutton and C.H. Behroozi, Nature, 397, 594-8 (1999) J.P. Marangos, ibid, 397, 559-560 (1999).
[5] K.M. Gheri, P. Grangier, J-P. Poizat and D.F. Walls, Phys. Rev. A 46, 4276-4285 (1992).
[6] S.E. Harris, J.E. Field and A. Imamoglu, Phys. Rev. Lett., 64, 1107-1110 (1990); G.Z. Zhang, K. Hakuta and B.P. Stoicheff, Phys. Rev. Lett 71, 3099 (1993); A. J. Merriam, S.J. Harpe, H. Xia, D. Manuszak, G.Y. Yin and S.E. Harris, Opt. Lett. 24, 625 (1999); C. Dorman, I Kucukkara and J.P. Marangos, Phys. Rev. A, 61, 013802 (1999).
[7] A.D. Greenstreet, C. Wei, S.A. Holmstrom, J.P.D. Martin, N.B. Manson, K.R. Catchpole and C. Savage, J.Opt.B: Quantum Semiclass. Opt. 1, 240-244 (1999); A.D. Greenstreet, C. Wei and N.B. Manson, Phys. Rev. A 59, 1-4 (1999).
[8] S.N. Sandhiya and K.K. Sharma, Phys. Rev. A 55, 2155-2158 (1997).
[9] S.M. Sadeghi, J. Meyer and H. Rastegar, Phys. Rev. A 56, 3097-3105 (1997).
[10] C. Wei, D. Suter, A.S.M Windsor and N.B. Manson, Phys. Rev. A, 58, 2310 (1998).
[11] M.D. Lukin, F.R. Hammer, M. Loffler and M.O. Scully, Phys. Rev. Lett., 81, 2675-2678 (1998); M.D. Lukin, A.B. Matsko, M. Fleischhauer and M.O. Scully, Phys. Rev. Lett., 82, 1847-1850 (1999); A.F. Huss, N. Peer, R. Lam-megger, E.A. Korunksky and L. Windholz, Phys. Rev. A 63, 013802.
[12] A. Imamoglu, H. Schmidt, G. Woods and M. Deutch, Phys. Rev. Lett., 79, 1467 (1997); S. Rebić, S.M. Tan, A.S. Parkins and D.F. Walls, J. Opt. B: Quantum Semiclass. Opt. 1, 490 (1999); K.M. Gheri, W. Alge, and P. Grangier, Phys. Rev. A 60, R2673 (1999); A.D. Greenstreet, J.A. Vaccaro, S.R. de Echaniz, A.V. Durrant and J.P. Marangos, J.Opt. B: Quantum Semiclass. Opt 2, 252-259 (2000).
[13] D.J. Fulton, S. Shepherd, R.R. Mosley, B.D. Sinclair and M.H. Dunn, Phys.Rev.A 52, 2302-2310 (1995).
[14] H.Y. Ling, Y-Q. Li and M. Xiao, Phys. Rev. A 53, 1014-1026 (1996).
[15] A.M. Akulshin, S. Barreiro and A. Lezana, Phys. Rev. A 57, 2996 (1998); A. Lezana, S. Barreiro and A.M. Akulshin, Phys. Rev. A 59, 4732-4735 (1999); V.M. Entin, I.I. Ryabtsev, A.E. Boguslavskii and I.M. Beterov, JETP Lett., 71, 175-177 (2000); A.V. Taichenachev, A.M. Tu-maikin and V.I. Yudin, Phys. Rev. A 61, 011802-1-4.
[16] D. McGlin, M.H. Dunn and D.J. Fulton, Phys. Rev. A, 62, 053802 (2000).
[17] B. W. Shore, The theory of coherent atomic excitation, volume 2, Multilevel atoms and incoherence, (John Wiley and Sons, New York, 1990).