Coded Caching and Spatial Multiplexing Gain Trade-off in Dynamic MISO Networks

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Abstract—The global caching gain of multi-antenna coded caching techniques can be also mostly achieved in dynamic network setups, where the cache contents of users are dictated by a central server, and each user can freely join or leave the network at any moment. In the dynamic setup, users are assigned to a limited set of caching profiles and the non-uniformness in the number of users assigned to each profile is compensated during the delivery phase by either adding phantom users or serving a subset of users with unicast transmissions. In this paper, we perform a thorough analysis and provide closed-form representations of the achievable degrees of freedom (DoF) in such hybrid schemes, and assess the inherent trade-off between the global caching and spatial multiplexing gains caused by either adding phantom users or serving parts of the data through unicasting.

Index Terms—coded caching; dynamic networks; multi-antenna communications

I. INTRODUCTION

With the increasing volume and variety of multimedia content, wireless networks are constantly being challenged for supporting higher data rates and lower latency [1]. Especially, new wireless immersive viewing application, as one of the expected key 6G drivers, will push network capabilities beyond what’s achievable by current state of the art [2], [3].

The work of Maddah-Ali and Niesen proposed coded caching as a method of leveraging cache content across the network to promote efficient delivery of such multimedia content [4]. Coded caching boosts the achievable rate by a multiplicative factor proportional to the cumulative cache capacity in the entire network through multicasting carefully designed codewords to diverse groups of users. Given the significance of multi-antenna communications in the evolution of next-generation networks [1], the cache-aided multiple-input single-output (MISO) configuration was later investigated in [5], [6], revealing that the same coded caching benefit could be accomplished alongside the spatial multiplexing gain.

Many later research works in the literature addressed critical scaling and performance challenges raised by singleand multi-stream coded caching mechanisms. For example, optimized beamformer design for improving the finite signal-to-noise-ratio (SNR) performance of MISO systems was discussed in [7], [8], while the subpacketization issue (i.e., the number of smaller parts each file should be split into) was studied in [9], [10]. Moreover, adapting coded caching to location-dependent file request scenario was considered in [2], and increasing the caching gain with receiver-side multiple antennas was studied in [11].

Another critical impediment to implementing coded caching techniques is their reliance on prior knowledge of the number of users for determining the cache contents at each user, making the implementation challenging in dynamic networks where the users can freely join and leave the network. Although fully decentralized schemes are able to address this issue partially [12], their achievable gain approaches the one of classical centralized schemes only when the number of users or files tends to infinity. Another approach is to use hybrid centralized/decentralized approaches that aim to compensate for network dynamicity with a controlled degrees of freedom (DoF) loss [13], [14]. Especially, for MISO links, the idea is to assign users to a limited number of caching profiles, resulting in a shared-cache setup as studied in [15].

In this work, we specifically consider the hybrid scheme in [14] that compensates for the non-uniformness in the number of users assigned with each profile by either adding virtual, phantom users or excluding a subset of excess users from multicast transmission and instead serving them with multi-user unicast beamforming in an orthogonal resource block. In this scheme, the delivery phase comprises two consecutive steps that deliver parts of data through coded caching techniques and unicasting, thus enabling a trade-off between the global caching and spatial multiplexing gains. While the work in [14] considers the finite-SNR communication regime and uses numerical simulations to show the small performance gap with the uniform, centralized case, it lacks a proper theoretical analysis of the achievable DoF. In this regard, here we perform a thorough analysis and provide closed-form representations of the achievable DoF of the scheme in [14], clarifying the real DoF loss with respect to the uniformly distributed users case, and the inherent trade-off caused by adding phantom users or serving parts of data with orthogonal unicast transmissions.

Throughout the paper, we use boldface lower- and uppercase letters to denote vectors and matrices, respectively. Sets are shown with calligraphic letters. $\mathbf{A}[i, j]$ is the element at row $i$ and column $j$ of matrix $\mathbf{A}$, and $\mathbf{a}[i]$ is the $i$-th elements of vector $\mathbf{a}$. $[K]$ represents the set $\{1, 2, ..., K\}$.
Fig. 1: System model of the considered dynamic scheme at a sample time instant: Users \( \{1, 2, 3, 4\} \) are present and do not leave the network, users \( \{7, 8, 9\} \) are joining, and users \( \{5, 6\} \) are leaving the network. Here, \( p[k] \) is the profile that user \( k \) is assigned to, e.g., user 1 is assigned to profile 2.

II. CODED CACHING FOR DYNAMIC MISO SETUPS

A. System Model

As discussed in [14], we consider a MISO setup where a multi-antenna transmitter serves a set of cache-enabled users. The transmitter can support a maximum spatial multiplexing gain of \( \alpha \), and has access to a library \( \mathcal{F} \) of some equal-sized files. The cache memory at each user is large enough to store a portion \( 0 < \gamma < 1 \) of the entire library. We assume \( \gamma = \frac{1}{r} \), where \( r \) and \( P \) are natural numbers and \( \gcd (r, P) = 1 \). The users are free to join and leave the network at any moment. Upon joining the network, the user \( k \) is assigned with a cache profile \( p(k) \in \mathcal{P} \), and its cache contents are updated following a content placement algorithm. A graphical representation of the system model is presented in Figure 1.

The dynamicity of the networks results in a varying number of users in the network during the time. At given time intervals, the users present in the network reveal their requested files (from the library \( \mathcal{F} \)) to the transmitter. The transmitter then builds and transmits a set of codewords following a content delivery algorithm, such that after the transmissions are concluded, all the users can decode their requested contents. In this paper, we consider the delivery process in a specific time interval with \( K \) total users in the network, and assume the same process is repeated in each interval. Following the general approach in the literature, we consider the total DoF, defined as the average number of users served simultaneously during each interval, as the performance metric.

B. Content Placement

Upon joining the network, every user \( k \in [K] \) is assigned with a caching profile \( p(k) \), where \( p(k) \in \mathcal{P} \). Cache contents of user \( k \) follow its assigned profile. Let us define a \( P \times P \) binary placement matrix \( \mathbf{V} \), for which: a) in the first row, the first \( \lfloor \frac{1}{r} \rfloor \) elements are one and the rest are zero, b) the row \( p \), \( 1 < p \leq P \), is a circular shift of its previous row to the right. Then, we split each file \( W \in \mathcal{F} \) into \( P \) equal-sized packets \( W_p \), and if \( \mathbf{V}[p, p(k)] = 1 \) for some row index \( p \) and user index \( k \), store \( W_p \) in the cache memory of user \( k \) for every file \( W \in \mathcal{F} \). Note that multiple users may be assigned with the same profile, and hence, have similar cache contents.

For the considered time interval, we assume the number of users assigned with profile \( p \) is \( \eta_p \), and \( \sum_p \eta_p = K \).\(^1\)

\(^1\)During each time interval, depending on the number of users leaving or joining the network, \( \eta_p \) and \( K \) values vary.

C. Content Delivery

Following [14], content delivery for the considered dynamic network setup comprises two consecutive steps. Here, we first briefly review each step, and then, clarify the whole process in Example 1.

1) Coded Caching (CC) data delivery

In this step, the server first selects a unifying profile length parameter \( \hat{\eta} \), and then, assuming \( \hat{\eta} \) users are assigned to each profile, builds and transmits a set of codewords using a novel coded caching scheme. We discuss the effect of the parameter \( \hat{\eta} \) on the DoF in the next section. In order to assume a uniform profile assignment, for every profile \( p \),

- if \( \hat{\eta} < \eta_p \), we randomly\(^2\) select \( \eta_p - \hat{\eta} \) users assigned with profile \( p \) and exclude them from the CC data delivery step. These users are then served during the subsequent step;
- if \( \hat{\eta} \geq \eta_p \), we add \( \hat{\eta} - \eta_p \) phantom users, which are imaginary, non-existent users, and assign them to profile \( p \).

The codeword building process follows a similar approach to the RED scheme in [10]. First, we consider a virtual MISO network with the spatial DoF \( \bar{\alpha} = \lfloor \alpha / \hat{\eta} \rfloor \) where each of the \( P \) caching profiles is treated as a virtual user (thus resulting in the coded caching gain \( \bar{\gamma} = P / \alpha \)). Then, we use the RED scheme in [10] to create transmission vectors for the virtual network, resulting in \( P \) transmission rounds each with \( P - \bar{\gamma} \) transmissions. We use \( \mathbf{x}_j^p \) to denote the virtual transmission vector \( j \) at round \( r \), and \( \mathbf{K}_j^p \) to represent the set of virtual users (profiles) served by \( \mathbf{x}_j^p \). Finally, we elevate every virtual transmission vector \( \mathbf{x}_j^p \) and remove the effect of the phantom users to yield the transmission vectors for the original network.

Creating transmission vectors for the virtual network follows a cyclic delivery algorithm and is explained in detail in [10]. We revisit this procedure in the next section while calculating the DoF. However, during the elevation process, we elevate each virtual transmission vector into \( \hat{\eta} \) transmission vectors for the original network\(^3\) by replacing each virtual user with either \( \hat{\eta} \) or \( b \) users, depending on the value of \( b = \alpha - \hat{\eta} \lfloor \alpha / \hat{\eta} \rfloor \), and removing or suppressing the inter-stream interference for these users with spatial multiplexing. For every user \( k \) replacing a virtual user \( \hat{\eta} \) we have \( p(k) = \hat{k} \), and hence, we use the term caching profile interchangeably with the virtual user index while discussing the elevation process. As discussed in [14], during elevation, we also need to further split each packet into \( p = \hat{\eta} + \alpha \) smaller subpackets.

2) Unicast (UC) data delivery

In this step, the server transmits all missing data excluded from the CC data delivery phase (i.e., the data requested by users excluded when \( \hat{\eta} < \eta_p \) for some profile \( p \)). At this step,

\(^2\)In practice, we may get an improved performance by excluding users with poor channel conditions.

\(^3\)In [14], it is suggested that if \( \frac{\alpha}{\hat{\eta}} \) is an integer, each virtual vector can be elevated into only one vector for the original network. This suggestion reduces the required subpacketization by a factor of \( \hat{\eta} \) but complicates the DoF analysis.
only the local caching gain is available together with the spatial multiplexing gain, and there is no global caching gain as in the CC delivery step.

Let us assume the number of users being served in this step is $K_U$. We split each file requested by these users into the same number of subpackets as in the CC delivery step. As the cache ratio at each user is $\gamma$ and the total subpacketization is $F\rho$, each user needs to receive (at most) $F\rho(1-\gamma)$ subpackets to decode its requested file. To deliver the missing subpackets, we use a greedy algorithm in which we: 1) sort the users by their number of missing subpackets, 2) build a transmission vector that delivers one missing subpacket to each of the first $\alpha$ users (or all the remaining users, if $K_U < \alpha$) using spatial multiplexing, and 3) repeats the whole procedure until all the subpackets are delivered.

**Example 1.** Consider a MISO network with $\alpha = 4$ and $\gamma = \frac{1}{3}$ (i.e., $P = 3$ and $t = 1$). The placement matrix $V$ and the cache files are assigned with the first profile (shown by $\mathcal{Z}(1)$) are given as

$$V = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 0 \end{bmatrix}, \quad \mathcal{Z}(1) = \{ W_1 \mid W \in \mathcal{F} \}.$$

Let us assume that in the considered time instant, eight users are in the network, and users $\{1, 2\}, \{3, 4, 5\}, \{6, 7, 8\}$ have been assigned with the first, second, and third profiles, respectively. For this network, we briefly review the delivery process for $\hat{n} = 2, 3$. As $\bar{\alpha} = \lfloor \alpha / \hat{n} \rfloor$, for both cases we have $\bar{\alpha} = 2$. Then, the virtual network will have $P = 3$ virtual users, coded caching gain $\bar{t} = 1$, and spatial multiplexing gain $\bar{\alpha} = 2$. Using the RED scheme in [10], the packet index vector for the first transmission in the first round for this virtual network is $\mathbf{k}^1 = [1 \ 2 \ 3]$, and the respective virtual transmission vector is

$$\tilde{x}_{1,1}^1 = W_2^2 (1) \tilde{w}_3 + W_3^2 (2) \tilde{w}_3 + W_4^3 (3) \tilde{w}_2,$$

where $\tilde{W}$ ($\tilde{k}$) denotes the virtual file requested by virtual user $k$, superscripts show the subpacket index, and $\tilde{w}_k$ is the optimized beamformer suppressing its associated data term at virtual user (profile) $k$.

Now, if $\hat{n} = 2$, we don’t need to add any phantom users but should exclude two real users assigned with the second and third profiles. Let us assume users 5 and 8 are excluded. Then, the first transmission vector resulting from elevating $\tilde{x}_{1,1}^1$ is

$$\tilde{x}_{1,1}^1 = W_2^2 (1) \tilde{w}_{6,7,2} + W_3^2 (2) \tilde{w}_{6,7,1} + W_4^3 (3) \tilde{w}_{6,7,4} + W_5^4 (4) \tilde{w}_{6,7,3} + W_6^4 (6) \tilde{w}_{3,4,4} + W_6^4 (7) \tilde{w}_{3,4,4}.$$

The excluded users 5 and 8 are then served in the UC step, which requires $P(\hat{n}+\alpha)(1-\gamma) = 12$ transmissions each delivering one subpacket in parallel to both users 5 and 8.

However, if $\hat{n} = 3$, we need to add one phantom user and assign it to the first profile, but no user is excluded from the CC delivery step (and hence, there is no UC step). Let us assume the phantom user 1 is assigned to the first profile. Then, the first transmission vector resulting from the elevation of $\tilde{x}_{1,1}^1$ is

$$\tilde{x}_{1,1}^1 = W_2^2 (1) \tilde{w}_{6,2,1} + W_3^2 (2) \tilde{w}_{6,1,1} + W_4^3 (1) \tilde{w}_{6,1,2} + W_5^4 (3) \tilde{w}_{6,4,5} + W_6^4 (4) \tilde{w}_{6,3,5} + W_6^4 (5) \tilde{w}_{6,3,4} + W_6^4 (6) \tilde{w}_{3,4,5}.$$

which, after removing the effect of the phantom user 1 is equivalent to

$$\tilde{x}_{1,1}^1 = W_2^2 (1) \tilde{w}_{6,2,1} + W_3^2 (2) \tilde{w}_{6,1,1} + W_4^3 (3) \tilde{w}_{6,4,5} + W_5^4 (4) \tilde{w}_{6,3,5} + W_6^4 (5) \tilde{w}_{6,3,4} + W_6^4 (6) \tilde{w}_{3,4,5}.$$

Let us consider the decoding process at user one, after the transmission of $\tilde{x}_{1,1}^1$ in [4]. Following the cache placement process, interference terms $W_1^1 (3), W_1^4 (4), W_1^5 (5), W_1^6 (6)$ are all available in the cache memory of user one and could be removed from the received signal. On the other hand, $W_2^2 (2)$ is also suppressed at user one with beamforming, and hence, this user can decode $W_2^2 (1)$ interference-free.

The transmission process for both cases of $\hat{n} = 2, 3$ is depicted in Figure 2. Comparing equations (2)-(4), we can see that without phantom users, the DoF value of the CC step is fixed and limited, but we need to deliver part of the data in the UC step (which hurts the total DoF). On the other hand, by increasing $\hat{n}$, a few users will be served in the UC step, but the DoF in the CC step varies in each transmission.

**III. DoF Analysis**

As mentioned in Section II-A, we define DoF as the average number of users served simultaneously during the whole content delivery phase. However, as every target user is receiving exactly one subpacket during each transmission, we may also equivalently calculate the average number of transmitted subpackets instead. In this regard, defining $J_M$ and $J_U$ to be the total number of transmitted subpackets, and $T_M$ and $T_U$ to denote the total number of transmissions at CC and UC delivery steps, respectively, the DoF is calculated as

$$\text{DoF} = \frac{J_M + J_U}{T_M + T_U}.$$

Let us also define $K_M$ and $K_U$ to be the number of users being served in CC and UC data delivery steps, respectively. In other words, given the $\hat{n}$ value, we have $K_M = \sum_p \min(\hat{n}, \eta_p)$ and $K_U = \sum_p \max(\eta_p - \hat{n}, 0)$.

In order to compute the DoF, we need to know the number of times each virtual user (or equivalently, each profile) is served during the CC data delivery step. Lemma 1 provides us with that.
Lemma 1. Each virtual user appears \((P - \bar{i})\) times as the \(m\)-th element, \(m \in [\bar{i} + \bar{\alpha}], \) in all user index sets \(\bar{k}^r_j, \ r \in [P]\) and \(j \in [P - \bar{i}].\)

Proof. From \([10]\), we know that for every round \(r \in [P]\) and transmission index \(j \in [P - \bar{i}], \) \(\bar{k}^r_j \) is calculated as

\[
k^r_j = \left[ r : (r + \bar{i} - 1) \mod P \right];
\]

\[
\left( \left[ (r : (r + \bar{i} - 1) \mod (P - \bar{i})) + \bar{i} \right] \mod P \right).
\]

Let us consider a fixed round \(r = p\). Clearly, the first element of \(\bar{k}^r_j \) is \(p\), and as \(\bar{k}^{r+1}_j = (\bar{k}^r_j + 1) \mod P, \) the second element of \(\bar{k}^{r+1}_j \) is also \(p\). Similarly, as for a fixed \(j\) each \(\bar{k}^r_j \) is a circular shift of \(\bar{k}^r_j, \) the first element of \(\bar{k}^r_j \) is the \((r - p) \mod P + 1\)-th element of \(\bar{k}^r_j.\) As a result, for a fixed \(j, \) the first element of \(\bar{k}^r_j \) equally places as the \(r\)-th element of \(\bar{k}^r_j \) during all the \(P\) rounds of transmissions. On the other hand, since \(j\) varies from one to \((P - \bar{i}),\) the number of times that the first element of \(\bar{k}^r_j \) (and equivalently each virtual user) appears as the \(m\)-th element of all user index sets \(\bar{k}^r_j \) is equal to \((P - \bar{i}).\)

Theorem 1. The DoF of the proposed scheme in a network with spatial multiplexing gain \(\alpha,\) cache ratio \(\gamma,\) and the unifying profile length parameter \(\bar{\eta} \) is equal to

\[
\text{DoF} = \begin{cases} 
K_M \bar{\eta} + \frac{K_M \alpha}{\bar{\eta}^2} & \text{if } K_U = 0 \\
K_M ((P - \bar{i})(\bar{\eta}^2 + \alpha) + K_M (P - \bar{i})(\bar{\eta}^2 + \alpha)) & \text{if } K_U < \alpha \\
K_M ((P - \bar{i})(\bar{\eta}^2 + \alpha) + K_M (P - \bar{i})(\bar{\eta}^2 + \alpha)) & \text{if } K_U \geq \alpha \\
\frac{P(P - \bar{i})\bar{\eta}^2 + \alpha}{P(P - \bar{i})\bar{\eta}^2 + \alpha} & \text{if } K_U = 0 \\
\frac{K_M \alpha}{\bar{\eta}^2} & \text{if } K_U < \alpha \\
K_M ((P - \bar{i})(\bar{\eta}^2 + \alpha) + K_M (P - \bar{i})(\bar{\eta}^2 + \alpha)) & \text{if } K_U \geq \alpha \\
\end{cases}
\]

Proof. We explicitly derive \(J_M, J_U, T_M\) and \(T_U,\) and then, use the DoF definition in \([\text{I}].\) In order to calculate \(J_M\) and \(T_M\) corresponding to the CC data delivery step, we recall that: 1) each user in the virtual network corresponds to a caching profile in the original network; 2) from Section \([\text{II}],\) every virtual transmission vector \(x^r_{\bar{\eta}, \bar{\delta}} \), \(j \in [P - \bar{i}],\) \(r \in [P],\) is elevated into \(\bar{\eta} \) transmission vectors \(x^r_{\bar{\eta}, \bar{\delta}}, \) \(\bar{\delta} \in [\bar{\eta}],\) for the original network; 3) following the discussions in \([\text{I}],\) the users connected to the first \((\bar{i} + \bar{\alpha} - 1)\) elements of \(\bar{k}^r_j \) are served with \(\bar{\eta} \) transmission vectors \(x^r_{\bar{\eta}, \bar{\delta}}, \) but the users assigned to the last element of \(\bar{k}^r_j \) are served only with \(\bar{\eta} \) transmission vectors \(x^r_{\bar{\eta}, \bar{\delta}} \) where \(\bar{\delta} \) is the remainder of the division of \(\alpha\) by \(\bar{\eta};\) 4) using Lemma \([\text{I}],\) every virtual user (i.e., profile index) appears \((P - \bar{i})\) times as the \(m\)-th element of user index sets \(\bar{k}^r_j, \) where \(m \in [\bar{i} + \bar{\alpha}].\) Now, since \(K_M\) users participate in the CC delivery step, the total number of transmitted subpackets at this step is obtained as

\[
J_M = K_M ((P - \bar{i})(\bar{\eta}^2 + \alpha) + \bar{\eta}(\bar{i} + \bar{\alpha} + \bar{\delta}), \quad \text{which, after substituting } \bar{\alpha} = \lceil \alpha/\bar{\eta} \rceil \text{ and } \bar{\delta} = \alpha - \bar{\eta} \lceil \alpha/\bar{\eta} \rceil, \text{ is reduced to}
\]

\[
J_M = K_M ((P - \bar{i})(\bar{\eta}^2 + \alpha)).
\]

In addition, as stated earlier, we have a total number of \(P(P - \bar{i})\) virtual transmission vectors, each elevated into \(\bar{\eta} \) vectors for the original network. Hence, the total number of transmission in the CC delivery step is equal to

\[
T_M = P(P - \bar{i}) \bar{\eta}.
\]
by exhaustive search). As observed, when \( \sigma \) is small, the maximum DoF can be easily achieved by setting \( \bar{\eta} = \max_p \eta_p \). In other words, when the users are distributed approximately uniformly among the profiles, a better DoF is achieved by involving more users in the CC delivery step. This is due to the fact that for near-uniform distributions of \( \eta_p \) values, setting \( \bar{\eta} = \max_p \eta_p \) does not require adding many phantom users, while selecting \( \bar{\eta} \) less than \( \max \eta_p \) would increase the number of excluded users, thus decreasing the coded caching gain and hurting the DoF. However, for large values of \( \sigma \) (e.g., \( \sigma = 30 \)), the maximum DoF can be achieved at \( \bar{\eta}/ \max \eta_p \approx 0 \) which demonstrates that it is better to serve all users in the UC step to achieve a higher DoF. This is due to the fact that for very non-uniform distributions of \( \eta_p \) values, selecting \( \bar{\eta} > 0 \) requires adding many phantom users and this hurts the DoF as their effects should be removed before the real transmissions.

It can also be observed from Figure 4 that the DoF is not a monotonic function of \( \bar{\eta} \). This demonstrates that there exists a trade-off between the CC and UC delivery steps, which can be balanced by carefully choosing the \( \bar{\eta} \) value.

In Figure 4 for every feasible distribution of \( \eta_p \) values, we have compared the best achievable DoF (found by line search over the \( \bar{\eta} \) value and shown by \( \text{DoF}_M \)) with the DoF of the optimal, uniform distribution (denoted by multicast only and shown by \( \text{DoF}_{opt} \)). For a better comparison, we have also included the achievable DoF when all the requested data is served using the UC delivery step only (i.e., without any coded caching gain).

As observed, the ratio \( \text{DoF}_M/\text{DoF}_{opt} \) decreases as \( \sigma \) is increased. This shows that increasing non-uniformness in the distributions of \( \eta_p \) values generally degrades the maximum achievable DoF with the proposed scheme. This was expected as both tools for compensating for the non-uniformness in \( \eta_p \) distribution (i.e., adding phantom users and excluding users from the CC step) hurt the DoF. However, for moderate non-uniformness in \( \eta_p \) values (e.g., \( \sigma \leq 10 \)), the proposed scheme enables a noticeable performance improvement (10-50 percent) over the full unicast method. The emphasizes the importance of employing various methods at the transmitter to make sure the distribution of \( \eta_p \) values is as uniform as possible, while switching to simple unicast methods when the non-uniformness increases.

V. CONCLUSION AND FUTURE WORK

We analyzed the degrees-of-freedom (DoF) of a hybrid decentralized/centralized coded caching scheme for dynamic setups where the users could freely join or leave the network at any moment. It was illustrated that increasing the non-uniformness in users’ distributions decreases the achievable DoF. Accordingly, in order to compensate for this non-uniformness, we either added some phantom users or served a subset of users with unicast transmissions which raised an inherent trade-off between the global caching and spatial multiplexing gains. In other words, for each users’ distribution, we should find the best unifying profile length to maximize the DoF of serving users with either multicast or unicast transmissions. Managing the trade-off between global caching and spatial multiplexing gain to find the optimal profile length is a subject of our future work.

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