High-throughput label-free flow cytometry based on matched-filter compressive imaging

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Abstract: We present a fast label-free computational flow cytometer based on a strategy of
compressive imaging. Scattered light from flowing objects is sub-divided into user-defined basis
patterns by a deformable mirror and routed to different detectors associated with each pattern.
The patterns can be optimized to be matched to the object features of interest, thus facilitating
object identification and separation. Compared to conventional scanning flow cytometers, our
technique provides increased information capacity without sacrificing flow velocity. Unique
features of our matched-filter strategy are that it can simultaneously probe multiple objects
throughout large fields of view with long depths of field. In our proof-of-concept demonstrations,
we achieve throughputs of over 10,000 particles/s, working at flow velocities of over 1 m/s.

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1. Introduction

Conventional flow cytometry uses fluorescent or scattered light to measure multiple parameters
of cells or organisms, which are used for identification and quantification [1]. Examples of its
broad biological and medical applications include disease diagnosis (such as Leukemia) [2],
quantifying waterborne bacteria in drinking water [3], and monitoring the immune status of
patients by measuring populations of immune cells [4].

Throughput and classification performance are two important properties that characterize flow
cytometry performance. However, tradeoffs exist. For example, the most common scanning
flow cytometers (SFC) based on light scattering measure only two parameters, the amount of
forward scatter (FS) and the amount of side scatter (SS) [5]. Analysis of these two parameters
can provide basic size and granularity information, which can be used for cell classification.
Since only two detectors are required, this type of flow cytometer can be very fast, allowing
flow velocities on the order of meters per second and very high throughput. However, since the
information contained in only two parameters is inherently limited, classification is generally
rudimentary and simultaneous processing of multiple objects is not achievable. A straightforward
way to improve classification performance is to increase the number of measured parameters.
This is the premise behind imaging flow cytometers (IFCs), which rely on a variety of imaging
techniques to acquire actual images of cells or organisms [6–10]. These images, which provide
thousands of signals (pixels), can significantly improve classification performance because of
their increased information content. However, IFCs are almost always based on the use of
cameras, which impedes system throughput due to lower frame rates. Even with the fastest
cameras available (frame rates in the kHz range), flow speeds of meters per second are completely
unattainable. To increase throughput, interesting variants of IFC have emerged making use of
spectral information in addition to spatial information [11,12]. For example, ultrafast IFC can
be obtained using time-stretch spectrometers, providing amplitude [13] or phase [14] images,
though at the cost of technical complexity. Moreover, the efficient reconstruction and analysis of
high dimensional image data can be challenging, requiring sophisticated algorithms [15–17] or
dedicated computational hardware [13].
An alternative strategy to increase information content involves not necessarily increasing the number of measured parameters, but increasing the information contained within each parameter, by making the parameters as orthogonal as possible. As an example, polarimetry-based flow cytometers measure the four orthogonal components of the Mueller matrix and achieve 200 cell/s throughput rates [18]. Another strategy combines pupil engineering with IFC [19], making use of filters in the pupil plane to selectively enhance sample features of interest. These are generally used in conjunction with cameras, since their applications generally do not require high throughput. Recently, the idea of matched-filtering has been applied with the use of a single-pixel camera [20], which is an example of compressive imaging [21,22].

In this work, we describe a label-free computational flow cytometer based on a similar concept of compressive imaging. We do not obtain the original images of our sample, but rather we detect a few (here four) parameters that are selected to enable optimal task-based classification of particular types of particles. This idea is a generalization of the single-pixel strategy presented in [20,23], except that instead of compressing the image to a single pixel, we compress it to a small number of pixels, so that we significantly increase the information content of each measurement without sacrificing acquisition speed.

![Schematics of the scattering patterns with fully and partially coherent illumination.](image)

Fig. 1. Schematics of the scattering patterns with fully and partially coherent illumination. Fully coherent laser illumination causes scattered light from different particles to interfere. With partially coherent illumination, patterns add linearly, facilitating the identification of multiple particles within a large FOV.

A unique feature of our design is that we use partially coherent illumination. Since coherence is needed for the generation of scattering patterns, FS/SS flow cytometers and scattering-pattern-based IFCs almost always make use of lasers, which provide fully coherent illumination [24,25]. But full coherence can lead to spurious interference between multiple particles within the field of view (FOV), confounding signal interpretation. In other words, full coherence limits the number of particles that can be monitored at any given time to a maximum of one. On the other hand, if the illumination is partially coherent, with coherence area only slightly larger than the particle size, then particles from different regions of the FOV produce scatter patterns that do not interfere but rather add linearly in intensity (See Fig.1). This property of linearity enables us to detect and identify multiple particles simultaneously within a much wider FOV without danger of crosstalk, thus allowing higher throughput. For example, we demonstrate count rates of over 10,000 particles/sec for two types of particles with high classification accuracy. Theoretically
we can achieve still higher throughput by further increasing the FOV and flow velocity, both of which are feasible.

2. Methods

![Schematic of our MFCI flow cytometry setup.](image)

Fig. 2. (a) Schematic of our MFCI flow cytometry setup. Dotted lines indicate conjugate object/image planes. For simplicity, the camera that images the DM plane is not shown. (b) Schematic of four basis patterns on the DM. Actuator tilts are applied such that each group of similarly tilted segments redirects light onto an associated detector/channel. (c) Image of the DM plane without the application of actuator voltages (i.e. flat). The size of the bright spot is an indication of spatial coherence range, controlled by the adjustable iris, which is adjusted here to focus most of the light power onto the central DM segment (ch1)

Our matched-filter compressive imaging (MFCI) flow cytometry setup is illustrated in Fig. 2, and is based on a standard widefield microscope design. A Thorlabs 625nm LED sends light through a 5× objective to provide transillumination. The spatial coherence area of the illumination is adjusted with a simple adjustable iris in the illumination Fourier plane, such that the illumination is fully coherent over the scale of the particles of interest, but incoherent across different particles. The scattered light produced by one or more particles is then collected by a 20× 0.46 NA Olympus objective. The scattering pattern is projected onto a pupil plane, where a reconfigurable deformable mirror (DM, Boston Micromachines Corp. Hex-1011) subdivides the pupil plane into four non-overlapping user-defined basis patterns. The DM mirror is comprised of 337 hexagonal segments, each supported by three surface-normal actuators that allow independent control of tip-tilt and piston. In other words, the light incident on each segment can be steered to an arbitrary direction [26]. The light incident on each of the four basis patterns is then routed to four different directions, specifically four different quadrants of a high-speed 2×2 array detector (quadrant detector, QD, SensL). Each quadrant integrates the incident intensity over a 6×6mm² area. To help equalize the signals, a square neutral density filter is placed in front of one of the quadrants (the one with the strongest signal, corresponding to ch1) to ensure that the detectors operate within their dynamic range. The signals are then independently amplified and acquired by a
4-channel high-speed data acquisition board (NI, PCI 6110). Downstream classification/counting is performed with only the signals from these four channels. In addition, to verify our result, a Thorlabs CCD camera is configured to directly image the flow channel. Flow is provided by a syringe pump (Harvard Apparatus) applied to a custom polydimethylsiloxane (PDMS) microfluidic flow channel, of transverse width 500 µm and axial depth 25 µm. The signals are first sampled at 5MHz, lowpass-filtered, and then downsampled to 200kHz to improve signal-to-noise ratio (SNR). Such temporal resolution can easily accommodate flow velocities on the order of m/s.

A key component of our MFCI strategy is the design of the non-overlapping matched filters in the detection pupil plane (i.e. the DM tilt patterns). In principle, an arbitrary pattern selection could provide signal diversity that could enable the separation of different particle types. However, to obtain optimal particle separability, a calibration procedure is prescribed. Such optimal separability is achieved when the matched-filter pattern minimizes the correlation between signals from different particle types. In other words, the optimal pattern depends on the specific features of the particle types of interest. In this work, proof-of-principle demonstrations are performed with polystyrene beads of diameters 6 µm and 10 µm (Polysciences, Inc.). Since the beads are circularly symmetric, the filters are also chosen to be circularly symmetric, in the shape of annuli of user-defined inner and outer radii. In order to calibrate our system, we performed a grid search with different combinations of annuli geometries and illumination iris sizes such that the signal changes caused by the two types of beads produced minimum linear correlation. This filter calibration process was relatively time-consuming. However, once optimized, the filters remained static. It should be noted that, once optimized, the DM could in principle be replaced by a low-cost interchangeable diffractive optical element (DOE). The advantage of using a reconfigurable DM here is that it facilitates the task-based filter search for fast prototyping.

Because of the linear property of our system, when multiple particles appear in the same FOV, the detected (intensity) signals are linear combinations of the signals generated by individual beads, which can be written as \( S(t) = T \cdot N_p(t) \), where \( N_p(t) \) is the number of particles at time \( t \) (here a \( 2 \times 1 \) vector), \( S(t) \) is the four signals measured at \( t \) (a \( 4 \times 1 \) vector), and \( T \) is the scattering matrix comprising the characteristic basis signals produced by each type of particle (a \( 4 \times 2 \) matrix). This linear relationship allows us to formulate the identification process as a straightforward linear inverse problem: \( N_p(t) = T^{-1}S(t) \). Though a simple pseudo-inverse can provide reasonable results, we also make use of a priori information. Specifically, the number of particles in the FOV is known to be a non-negative integer. We can impose this constraint on the least-squares computation to improve robustness. This problem is known as an overdetermined box-constrained integer least squares (OBILS) problem, and we applied the MILES algorithm [27] to perform the reconstruction. We note that MILES is fast when there are only two types of particles, though the efficiency is expected to decrease exponentially with increasing number of particle types (that is, OBILS is a NP-hard problem).

It should be emphasized that the accurate classification of multiple particles in the same FOV is not always straightforward. Conventional flow cytometers can only monitor single particles at a time and rely on a variety of techniques to prevent particle clustering [28]. With IFCs, the counting process can be done using computer vision or deep learning algorithms [29] at increased computation cost. Even so, frames with multiple/clustered particles are generally intentionally discarded to avoid erroneous readings [13].

3. Results

We begin by evaluating the performance of our MFCI flow cytometer with low flow velocity, in order to validate our data processing algorithms and classification accuracy. The raw signals are first corrected for background levels (measured with no particles in the flow channel), different amplifications and the ND filter, thus arriving at the corrected signals (\( S(t) \)). The characteristic
Fig. 3. (a) Corrected signals from the four channels. Conventional least square (LS) reconstruction is applied to the signals. Two traces representing the number of 6µm beads and 10µm beads are shown in (b) and (c), respectively. To the right of each trace is the corresponding histogram, showing that most numbers cluster about non-negative integers. (d) and (e) are the LS reconstruction results with non-negative integer constraint. (f) compares our reconstruction results with results obtained from ground truth images. Five example images (acquired by the CCD camera) are shown, associated with the red dotted lines in (d) and (e). A reconstruction is considered accurate when both number and types of beads are correct. We achieved 91% accuracy in this experiment.
vectors for each type of particle, embodied by the scattering matrix $T$, are predetermined from the calibration procedure. As explained above, $S(t)$ is a linear combination of the characteristic vectors weighted by the numbers of beads ($N_p(t)$). A simple least-square (LS) fit can be applied to $S(t)$ to infer the number and types of particles within the FOV (see Fig.3(b,c)). By plotting a histogram of each trace, we observe that the inferred numbers are clustered about non-negative integers, as expected. The LS results with non-negative integer constraint are also shown (Fig.3(d,e)), as are a set of ground truth images acquired by the CCD camera, provided for comparison (these ground-truth images are acquired at a very low velocity to obtain well-resolved images). We manually counted the numbers and types of particles in each ground-truth image and compared with the results obtained from reconstruction. The reconstruction results were found to be correct for 91% of the images (134 images were processed), where a discrepancy in either the number or type of particle constituted an error. In other words, our MFCI strategy provides a classification accuracy on par with image-based FC. To confirm that four detection channels provided greater classification accuracy than two channels, we attempted classification using only ch1 and ch2. This led to a poorer classification accuracy systematically worse than 40%.

But the key advantage of our MFCI strategy over image-based FC is its throughput. While IFC throughput is limited by the camera frame rate, in our case we use detectors that can operate well over MHz rates. We demonstrate this throughput advantage by increasing flow velocity (see Fig.4). Although our pump provides a constant debit (volume/sec), we found that the local flow velocity varied somewhat at different locations along the channel (laminar flow is assumed), presumably due to structural imperfections in our channel. A “findpeaks” function (MATLAB) was applied to the number-of-beads curve (LS with constraint) to obtain heights and widths of the peaks (Fig.4(a) – note that the 10µm beads were processed similarly though the data is not shown). A plot of the histogram of the peak widths allowed us to estimate the local average bead transit time to be 64µs. Since the transit length of our rectangular FOV is about 80µm, we estimate the local flow velocity to be about 1.25m/s, much faster than can be achieved with an IFC, and on par with flow velocities attained with conventional scanning FCs. Then we estimate the throughput of the system. This is done by simply summing the heights of all the peaks found earlier (see Fig.4(a)). The resulting throughput is over 10,000 particles/s. We confirmed that the concentration ratio of the two bead types (6µm:10µm) remained about 4.67, which is close to the ratio of 4.79 measured at slow flow velocity.

Yet another advantage of our MFCI strategy compared to an IFC relates to depth of field (DOF). Specifically, when particles are out of focus in an IFC, they become blurred. Such blurring hinders accurate classification and imposes severe constraints on the maximum channel depth. In our case, defocus leads to (quadratic) phase changes of the scattered field in the DM plane, not amplitude changes. While such phase changes, in turn, lead to a spreading of the signal powers at the detection plane, we are insensitive to such spreading because our detectors are large in area ($6 \times 6$mm$^2$). In other words, the measured signals are quite insensitive to defocus. To illustrate this advantage, we compared signals obtained with the quadrant detector and the camera when defocusing two static 10µm beads mounted on a slide. We reconstructed the number of beads using our MFCI procedure and compared this to the contrast (standard-deviation/mean) calculated in the red-circled area in the image stack. We note that these two curves do not strictly represent DOF but are close proxies that allow us to compare the robustness of each setup against defocus. We observe that image contrast almost completely disappears at 50µm defocus, meaning any image based classification/count algorithm would fail. In contrast, the particle number reconstructed by our technique continues to remain accurate, suggesting a much improved robustness against defocus and a capacity to work with channels even greater than 100µm in depth (in our demonstration, the channel depth was 25 µm). In other words, MFCI allows us to probe not only large sample areas, but also large sample volumes, enabling higher
throughput still. To illustrate this advantage, we compared signals obtained with the quadrant detector and the camera when defocusing two static 10μm beads mounted on a slide (see Fig. 5).

4. Conclusion

In summary, we have demonstrated a MFCI flow cytometer where basis pupil patterns are “matched” to the samples of interest. The technique combines the increased information capacity of image-based FCs with the increased throughput capacity of conventional non-image-based FCs. Specifically, a high throughput capacity is enabled not only by our use of fast detectors (as opposed to a camera), but also by the ability of our device to classify multiple particles within a same FOV. This last advantage comes from our use of partially coherent illumination (as opposed to laser illumination) designed to ensure signal linearity. Moreover, our system provides much larger DOF than image-based FCs, allowing the monitoring of particles throughout larger flow volumes, also facilitating higher throughput and enabling classifications rates of 10,000 particles/s with flow velocities of over 1 m/s.

One limitation of our technique is that the optimization of the basis patterns requires a labor-intensive search. In our proof-of-concept demonstration the problem was reduced to finding optimal sizes of the annulus-shaped DM patterns. However, designing optimized patterns becomes more challenging when the particles become more varied or structured. This problem is directly analogous to the kernel design problem in machine learning, where the goal is to maximally separate data in a high-dimensional space with as few coefficients as possible. In future work, we plan to derive basis pupil patterns using a machine learning model for automated optimization.

Our MFCI FC technique is conceptually simple and potentially low-cost. Here, we used a specialized tip-tilt DM to search for and apply our matched-filter patterns. In practice, this could
be done more cost-effectively with diffractive optics elements, pre-calibrated experimentally or designed based on a physical model of the scattering of interest. The simplicity of our device, along with its information capacity and throughput advantages, make it attractive for biomedical applications.

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