Dislocation-toughened ceramics

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Functional and structural ceramics have become irreplaceable in countless high-tech applications. However, their inherent brittleness tremendously limits the application range and, despite extensive research efforts, particularly short cracks are hard to combat. While local plasticity carried by mobile dislocations allows desirable toughness in metals, high bond strength is widely believed to hinder dislocation-based toughening of ceramics. Here, we demonstrate the possibility to induce and engineer a dislocation microstructure in ceramics that improves the crack tip toughness even though such toughening does not occur naturally after conventional processing. With modern microscopy and simulation techniques, we reveal key ingredients for successful engineering of dislocation-based toughness at ambient temperature. For many ceramics a dislocation-based plastic zone is not impossible due to some intrinsic property (e.g. bond strength) but limited by an engineerable quantity, i.e. the dislocation density. The impact of dislocation density is demonstrated in a surface near region and suggested to be transferrable to bulk ceramics. Unexpected potential in improving mechanical performance of ceramics could be realized with novel synthesis strategies.

Introduction

Ceramics are considered as inherently brittle. Widely accepted understanding states that a toughness-enhancing plastic zone in ceramics based on dislocations “would require changing the bond strength” which is “not a feasible undertaking”. In metals, in contrast, the availability of mobile dislocations results in high plastic deformability and fracture toughness. Although a large number of single crystalline ceramics can be deformed by dislocation movement at room temperature, dislocations have only rarely been connected to fracture toughness in ceramics. Instead, tremendous effort was focused on alternative mechanisms to toughen ceramics primarily in the 1980s. These efforts centered on shielding the crack tip from the applied load leading to a curve behavior where toughness is gained only after an advancement of the crack. This entails the dilemma that only long cracks create tough ceramics and, hence, only limited load-bearing capacity and low crack tolerance can be obtained.
In fact, it is strikingly easy to move dislocations in many ceramics even at cryogenic temperatures with evidence from indentation and single crystal compression (e.g. for LiF, MgO, SrTiO₃). Even though dislocations can move and ceramic single crystals are ductile, they, nevertheless, feature a low fracture toughness. Why?

Once dislocations are mobile, the ability of a material to nucleate dislocations at a crack tip is considered to be a further pre-requisite for a toughness enhancement by dislocations. While a nucleation of dislocations at crack tips readily occurs in metals and assures the supply of dislocations where needed, it occurs only to a very limited degree in ceramics (e.g. absent in SrTiO₃, see supplementary 1, ESI†). This results in the general belief that dislocations cannot toughen ceramics due to high bond strength and the inability to nucleate dislocations at crack tips at low temperatures.

Indications to the opposite are available but rare: MgO features dislocation activity at the crack tip at low crack velocity and a very high crack-tip toughness of \( K_0 = 9.8 \text{ MPa } \sqrt{m} \) under plane stress conditions in thin TEM samples. This value lies between typical toughness values for ceramics (e.g., Al₂O₃: \( K_c = 3 \text{ MPa } \sqrt{m} \)) and FCC metals (e.g., Aluminum: \( K_c = 30 \text{ MPa } \sqrt{m} \)).

But can a dislocation-based toughness-enhancing plastic zone be engineered into ceramics even though dislocations do not naturally nucleate at the crack tip? If so, this would allow new avenues for toughening ceramics and vastly expand applications. In particular it would empower us to combat short cracks and crack formation.

In the following, we demonstrate that the absence of local plasticity in ceramics does not hinge on bond strength but is intimately related to the availability of pre-existing dislocations in the volume around the crack tip (and grain boundary). Separation of motion and multiplication from nucleation allows us to predict that a high pre-existing dislocation density yields dislocation toughening. Subsequently we insert a high dislocation density of \( 5 \times 10^{14} \text{ m}^{-2} \) into the model material SrTiO₃ and demonstrate its impact both on local plasticity and toughness.

Dislocation-toughening

First, we quantify the influence of pre-existing dislocations on the stress intensity factor and relate to typical dislocation densities. In principle, the individual contributions of \( i \) (edge) dislocations on the stress intensity at a crack tip can be summed up \((\Sigma K_{Di})\) by factoring in the distance \( x_i \) from the crack tip as

\[
\Sigma K_{Di} = \sum_{i} \frac{\mu b}{(2\pi x_i)^{3/2}} \frac{\sqrt{1 - \nu}}{f(\phi_i, \theta_i)}.
\]

Here, \( \mu \) is the shear modulus, \( b \) is the Burgers vector, \( \nu \) the Poisson's ratio (107 GPa, 0.55 nm for the \{110\} \{\bar{1}10\} slip system and 0.237, respectively, for SrTiO₃), \( f(\phi_i, \theta_i) \) is a function of the angle between crack plane and slip plane \( (\phi_i) \) and the line joining the crack tip to the dislocation \( (\theta_i) \). The radius \( x \) of the plastic zone is rendered using the yield stress for SrTiO₃ \( \sigma_{YS} \) is 120 MPa and its pristine crack tip toughness, \( K_{0o} = 0.75 \text{ MPa } \sqrt{m} \) (as measured below) as

\[
x = \frac{1}{2\pi \left( \frac{K_{10}}{\sigma_{YS}} \right)^2} = 1.26 \mu m.
\]

Note that a typical dislocation density of \( 10^{10} \text{ m}^{-2} \) (see supplementary 2, ESI†) cannot provide toughening as statistically only 0.05 dislocations can be found in the area \( x \) at the crack tip explaining why natural toughening (i.e. by the pre-existing dislocations) is not typically observed. In contrast, if for example 500 dislocations were ideally oriented \((f(\phi, \theta) = 1)\) at a distance of \( x_i = 1.26 \mu m \), the sum of the toughening contribution would amount to \( \Sigma K_D = 13.7 \text{ MPa } \sqrt{m} \) (an 18-fold increase over \( K_{0o} \)). This would require a mobile dislocation density of \( 10^{14} \text{ m}^{-2} \).

A more precise description, adding substantial complexity, would need to take into account the exact arrangement of dislocations which are rearranged by the stress field of the crack tip. This simple realization already reveals that, for most ceramics, a dislocation-based plastic zone is not hindered by an insurmountable intrinsic property (bond strength) but by an engineerable quantity, which is the dislocation density.

Dislocation structure

Being aware of the necessity of high dislocation densities, we investigate the dislocation structure at a microscopic level with the ultimate goal of finding guidelines for engineering dislocation microstructure. We will elaborate how dislocations in ceramics propagate, multiply and nucleate (demonstrated using SrTiO₃ as model material).

Select ceramic single crystals, with the room temperature \( \{110\}\{110\} \) slip system of SrTiO₃ as well studied example, can be extensively deformed by uniaxial compression which enhances dislocation density. Dislocations arrange in slip bands with a density of \( 2 \times 10^{13} \text{ m}^{-2} \) (see Fig. 1a) on parallel slip planes. This behavior is well investigated also for LiF as well as other ceramic single crystals.

Dark-field X-ray microscopy (DFXM) allows monitoring dislocations inside of slip bands formed by deformation within a 200 \( \mu m \) thick bulk sample providing insight in the mechanisms of deformation. In order to not obscure DFXM images with natural dislocations (and exclude their effect), SrTiO₃ single crystals grown by top seeded solution growth with particularly low natural dislocation density were used for DFXM. In supplementary 3 (video, ESI†) the sample is tilted in various angles using topo-tomography. At the tip of a band, where the spacing is large, individual dislocations can be discerned clearly (Fig. 1b).

A large number of dislocation lines can be observed to link up between several lattice planes, best visible in 3D at slight tilt (see Fig. 1b and supplementary 3 (video, ESI†)). The slip band can be identified as a complex structure that extends almost equally in two dimensions and has a certain width in the third dimension. Here, several sites of multiple cross slip (each larger...
than 20 µm) can be observed due to the large field of view, see Fig. 1b. The cross slip enables Koehler sources, a multiplication mechanism creating new dislocations of same and opposite line vector on adjacent lattice planes.\(^{27,28}\) From three-dimensional data on strain and mosaicity (lattice tilt, see supplementary 4–7, ESI\(^*\)) acquired by layered imaging, we conclude that the strain fields overlap locally with no long-range strain fields around the bands. Additionally, we note the abundance of dislocation multiplication while we find no evidence for dislocation nucleation.

A contrast of DFXM images with TEM images allows verifying the mesoscopic dislocation structure observed inside of a band over a scale of hundreds of µm. This comparison confirms that the volume was, in fact, previously free of dislocations. Ultra-high voltage electron microscopy (UHVEM) is used to identify the dislocation orientation. In regions close to the slip band front with low dislocation density, edge-type dislocations on \(<110\>\{110\}\) planes with \(b = [110]\) Burgers vector are predominantly found. Furthermore, the dislocation propagation direction, \(\langle 110\rangle\), can be inferred from the orientation of the dipoles dragged behind jogs in Fig. 1c.\(^{25,26}\) Further behind the tip, the dislocation structure becomes much more complex and reveals more screw and mixed components (Fig. 1d).

A more detailed investigation by HAADF-STEM focused on a FIB-lamella from a slip band reveals dissociation of dislocations into twopartials\(^{11,21}\) (see supplementary 9, ESI\(^*\)). The configuration is climb-dissociated (see supplementary 10 (ESI\(^*\)) and Fig. 2a and b) with a climb distance of three unit cells, which is most likely induced by the electron beam activation. Approximately half of the 13 dislocations investigated at atomic resolution were found in a dipole configuration consisting of two dislocations dissociated into two partials each (see Fig. 2c and d). The distance between the dipoles, is less than 15 unit cells (Fig. 2d). When the temperature is sufficient for climb dissociation, recombination of the dipoles should be possible with similar thermal activation. Since dislocation dipoles are also known as origin of dislocation multiplication,\(^{25,29}\) a recombination is expected to hinder dislocation multiplication. The temperature range for recombination is found to coincide with the ductile to brittle transition in SrTiO\(_3\)\(^{11,30}\) as the amount of dislocations in a deformed crystal is significantly reduced when annealing at 900 °C (see supplementary 11, ESI\(^*\)).

In the following, we use molecular dynamics simulations to extend the picture of dissociated \(\langle 110\rangle\{110\}\)-type dislocations from a static observation after deformation to a mechanistic insight into dislocation structure evolution (for details see supplementary 12 (ESI\(^*\))\(^{31,32}\)). A model experiment\(^{13}\) provides a local stress concentration under compressive loading and yields well defined mobile dislocations in pure SrTiO\(_3\). As expected, we observe edge dislocation partials nucleating at surface defects. These dislocations propagate easily through the material under applied compressive forces.\(^{28,29}\)
stress. However, dislocations rarely traverse the crystal in a completely straight line, see supplementary video 13 (ESI†). In fact, the modeled dislocation segments climb spontaneously changing their glide plane by one atomic layer. In turn, the partial dislocations climb which gives rise to a new field of creating local defects (e.g. vacancies) and dislocation multiplication mechanisms. Examples for spontaneous climb and a dislocation multiplication during dislocation motion are given in Fig. 2e and f, respectively. A closer inspection of the dissociated dislocation reveals that climb dissociation is energetically favored over glide dissociation (Fig. 2h).30,34

Quantification of toughening

A proof-of-concept for dislocation toughening of ceramics requires a suitably high dislocation density. To engineer dislocation densities beyond $10^{14} \text{ m}^{-2}$, we apply a simple polishing procedure (Jin et al.35), which, however, impacts only a surface layer of about 5 μm. The statistic nature of point contacts of polishing particles with the surface abundantly nucleates dislocations and activates all available $\langle 110 \rangle$ type slip systems.10 Toughening in this thin layer is assessed in the following.

Deforming a volume with engineered high dislocation density only requires dislocation mobility but not dislocation nucleation. The locally increased plasticity can easily be verified using nanoindentation.9,10 For a dislocation-free volume, elastic behavior up to the theoretical shear stress is observed before a transition to elasto-plastic behavior. As this ‘pop-in’ occurs at ~17 GPa in Fig. 3a, dislocations are nucleated homogeneously for sharp indenters16 (see Fig. 3a and b). Appropriate choice of tip radius defines the probed volume with radius equal to $x$ of the plastic zone calculated in eqn (2).5,10 If a sufficient density of dislocations can be provided (see Fig. 3c and d), plastic flow sets in far below

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**Fig. 2** Dislocation structure at atomic resolution. (a) HAADF image of the dislocation core of a $\langle 110 \rangle$ $\langle 110 \rangle$ type dislocation with Burgers circuit. (b) Atom planes corresponding to (a), illustrating that the partial dislocations have climb-dissociated (see supplementary 10, ESI†), likely due to the electron beam. (c) Dislocations in close vicinity with less than 15 unit cells distance revealing opposite line vectors. (d) Atom planes corresponding to (c). (e) Molecular dynamics simulations highlight spontaneous climb of a dislocation and creation of a defective region with vacancies. Dislocation lines are indicated in orange and the direction of the Burgers vector as red arrow. (f) One of two dislocation partials climbs to a parallel (secondary) glide plane while the other stays on its original (primary) plane. New partials spawn to complete the singular partials. On the lower plane an extended stacking fault is created between the partials which is relieved by creating further partial dislocations effectively multiplying the dislocation. (g) Representation of a SrTiO$_3$ unit cell. The blue shapes represent polyhedra of oxygen around titanium and are well suited to identify defects such as stacking faults. For clarity the oxygen atoms are not shown in (e) and (f). (h) Dependence of the energy of two partial dislocations on their separation distance in climb dissociation. Partial dislocations of the shown type have a tendency to climb, see (a–d) as well as (e) and (f), which is energetically favored over dissociation in slip direction. For full details see Supplementary 12 (ESI†). (a–d) reprinted with permission from Porz, et al., ACS Nano, DOI: 10.1021/acsnano.0c04491. Copyright (2020) American Chemical Society.
dislocation density. A pristine SrTiO3 single crystal produces load, cracks were confined to the surface layer thickness with high indenting on a (100) surface with a Vickers indenter using 98.1 mN slip systems,35 see supplementary 14, ESI†

engineered surfaces (pristine surface) and 4g (toughened surface). The crack propagates from two corners of the indent which align with the {110} planes, see Fig. 4f and g. As this surface appears to be too tough for quantification in the dislocation-rich surface regime, an orientation with less toughening was considered.

On the (110) surface of SrTiO3, cracks originate from only two corners of the indent which align with the [110] planes, see Fig. 4f (pristine surface) and 4g (toughened surface). The crack propagation direction is, thus, least favorably oriented towards the available slip planes and is deemed to provide the smallest toughening effect. In consequence, the crack tip opening displacement method can be applied for quantification, because the ratio of crack length to indent diagonal is larger than two (Fig. 4f and g).

The crack tip toughness $K_{IC}$ is determined by fitting the initial square root-shaped crack opening displacement with the elastic displacement field for crack tips (see Experimental details). On the (110) surface, an increase of crack tip toughness beyond a factor of two from 0.75 MPa m$^{1/2}$ to 1.6 MPa m$^{1/2}$ is clearly related to the high dislocation density (see Fig. 4e). Our results demonstrate dislocation-induced toughening on two orientations of the model material SrTiO3 with an additional discussion on MgO in supplementary 17 (ESI†).

Discussion

While we observe an astonishing multitude of multiplication mechanisms at different length scales in addition to good dislocation mobility, we did not observe dislocation nucleation in the single crystals in uniaxial compression. Simultaneously we note that the dislocation density in both pristine single crystals and polycrystals (see supplementary 2, ESI†) is typically below $10^{14}$ m$^{-2}$. This renders volumes with the size of $10 \times 10 \times 10 \mu$m$^3$ (e.g. entire grains) dislocation-free. When attempting to deform a dislocation-free volume, instead of the shear stress required to move a dislocation (such as 60 MPa for SrTiO3) the stress to (homogeneously) nucleate a dislocation (such as ~17 GPa for SrTiO3, see Fig. 3) is required. Such nucleation step must be avoided.

The volume in a uniaxially compressed single crystal is typically large enough to find at least one dislocation which can move and multiply and, hence, nucleation is not required. In polycrystals instead, grain boundaries impede the motion
and each grain needs to be able to deform by itself, again requiring nucleation. The high nucleation stress\textsuperscript{10,39} then hinders a deformation of polycrystals. Accordingly the ductility observed in single crystalline ceramics is still often “surprising”\textsuperscript{7} or “unexpected”\textsuperscript{40}. However, as shown back in the 1960s, dislocation motion within some grains can lead to small but detectable macroscopic strains of polycrystalline ceramics\textsuperscript{41}, and even allows the formation of a plastic zone at crack tips (e.g. in MgO).\textsuperscript{42,43} The mechanical behavior of ceramics is then somewhat comparable to metals with extremely few dislocations.\textsuperscript{44} The formation of slip bands leads to nucleation of cracks at grain boundaries\textsuperscript{45} (also an origin of microcracking\textsuperscript{46}) because slip transfer or alternatively nucleation on the other side of the grain boundary (secondary slip) requires high stresses.\textsuperscript{39} This can substantially limit an effective plastic zone as observed e.g. for MgO.\textsuperscript{42,43} Furthermore, we suggest that the presence of dislocations or nucleation\textsuperscript{39} at grain boundaries are both more pressing and more easily addressable concerns for small strains than the Taylor criterion.\textsuperscript{45} Taylor suggested that at least five geometrically independent slip systems are required to deform a polycrystal due to the mismatch of random crystallite orientations. In ceramics, typically less than five slip systems are mobile at room temperature limiting the deformation of polycrystals.\textsuperscript{46} However, this neither limits large local deformation nor small macroscopic deformation.

We conclude that a high density of appropriately oriented and mobile dislocations is not only required for enhancing crack tip toughness but also to allow secondary slip on the other side of a grain boundary in order to avoid (micro)crack initiation by pile-up of dislocations in slip bands. In supplementary 18 (ESI\textsuperscript{†}), we demonstrate that slip band formation is suppressed by the dislocation structure. Furthermore, the provided dislocation structure substantially improves the cracking behavior of polycrystals (Fig. 5d and supplementary 19, ESI\textsuperscript{†}). From the investigation above we learn that multiplication of dislocations alone does not lead to desired dislocation structures. As fracture will prevail if local dislocation nucleation is required, dislocation toughening in ceramics is within reach but demands high dislocation densities.

**Steps for development**

The concepts discussed above open new perspectives for tweaking the mechanical performance of ceramics by dislocation-toughening. The impact of dislocations (Fig. 5a) can be readily assessed using a quantification of indentation pop-in (Fig. 5b) and a visual inspection of the tendency for cracking around the elastic-plastic indentation zone (Fig. 5c). Preliminary experiments suggest that the toughening effect can be transferred to polycrystals (see Fig. 5d).

For this new generation of dislocation-toughened ceramics, a high density of pre-existing dislocations (or suitable dislocation sources) is required, which calls for a rethinking of traditional processing strategies. While the effect in bulk polycrystals still awaits detailed investigations, the presented understanding will allow to make targeted efforts towards suitable processing strategies. Desirable dislocation structures could be achieved by plastic
deformation after processing, e.g. by local\(^2\) or high-pressure deformation.\(^{47}\) Fortunately, a suite of radically new densification techniques invented recently can result in a dislocation-rich microstructure. This could be the case, for example, for: (i) hydrothermal densification (cold sintering),\(^{48}\) (ii) the Aerosol Deposition Method (ADM)\(^{49}\) or (iii) ultrafast sintering based on rapid heating (e.g. flash sintering), resulting in ceramics with high dislocation density.\(^{50,51}\)

With dislocation densities of \(>10^{14} \text{ m}^{-2}\) revealed and already connected to improved mechanical behavior,\(^{34,52}\) there is considerable hope for applicability to bulk polycrystals.

**Conclusions**

We introduce the new concept of dislocation-toughening of ceramics by engineering a high dislocation density which enables formation of a crack tip plastic zone. High dislocation densities reduce the critical stress for plastic deformation by at least a factor of ten as assessed through a simple measurement of indentation pop-in. Concurrent enhancements of crack tip toughness by a factor of two have been obtained. The next step requires a synthesis method that efficiently introduces a sufficiently high dislocation density into the bulk ceramic. This has the potential to substantially toughen short cracks which may allow dramatically widening the application range of ceramics by increasing mechanical performance.

**Experimental**

**Crystal production and treatment**

Two different SrTiO\(_3\) materials were used: For succinct mapping of the 3-dim. mesoscopic dislocation structure the highest quality SrTiO\(_3\) single crystal, devoid of any prior dislocations was needed.

Towards this end, undoped top seeded solution grown single crystal SrTiO\(_3\) was produced at 1600 °C from TiO\(_2\) - rich solution by Daniel Rytz, FEE GmbH – A Division of EOT, Idar-Oberstein, Germany. The dimension was 1 \(\times 1.2 \times 2\) mm\(^3\) into which a notch was introduced with a 170 \(\mu\)m diameter diamond wire saw into the long side. Deformation was done using a load frame (2010, Zwick/Roell, Ulm, Germany) at room temperature in order to emanate slip bands from the notch but without the dislocations reaching the opposite free surface. Before deformation the surface was vibrationally polished. After deformation etching for 15–60 seconds in 15 ml 50% HNO\(_3\) with 16 drops of 48% HF was done. The thickness of the sample was reduced to 200 \(\mu\)m by grinding with Si\(_C\) sand paper.

In parallel, Verneuil-grown SrTiO\(_3\) single crystals (Alinaseon GmbH, Frankfurt am Main, Germany) were cut to dimensions of \(4 \times 4 \times 8\) mm\(^3\) containing a natural dislocation density of \(5 \times 10^{12} \text{ m}^{-2}\). These were then subjected to plastic deformation of 2% plastic strain. This material was used for TEM and indentation studies.

Pristine surfaces were prepared by careful polishing for 40 minutes with diamond particle size of 6 \(\mu\)m, 3 \(\mu\)m, 1 \(\mu\)m and then 1/4 \(\mu\)m and vibrational polishing for 15 hours with OP-\(S\) solution from Struers (Copenhagen, Denmark). This procedure removes all mechanically introduced dislocations and yields a pristine surface. A dedicated surface treatment referred to as “dislocation-inducing polishing procedure” in the text was developed to retain a high dislocation density at the surface but achieve the same pristine surface roughness. To this end, grinding with P2500 Si\(_C\) sandpaper introduced a maximized density of dislocations at the surface and the subsequent polishing time for each diamond particle polishing step was reduced to 30 seconds and vibrational polishing limited to 40 minutes. This removes a much thinner layer from the surface but flattens it. Both (100) as well as (110) surfaces were investigated.

**Mechanical testing at the surface**

Nanoindentation tests were carried out to assess the critical shear stress to initiate dislocation plasticity by quantifying the...
pop-in load. To this end the continuous stiffness measurement (CSM) mode was utilized with a constant strain rate of 0.05 s⁻¹ on the iNano system (Nanomechanics inc., USA) with a threesided Berkovich diamond indenter (Synton MDP, Switzerland). A maximum load of 45 mN was set, and a harmonic displacement oscillation of 2 nm was applied with a frequency of 100 Hz. For each indentation condition at least 10 tests were performed and later averaged. The frame stiffness and tip area functions were calibrated on a fused silica reference according to the Oliver-Pharr method.⁵³

Macroscopic indentation to introduce cracks was performed separately using a Vickers tip and 98.1 mN load. The crack tip toughness of short radial indentation cracks was quantified by determining the crack opening displacement as function of distance to the crack tip in a scanning electron microscope at magnification of 100 000 times. Vickers indentations of load 98.1 mN were placed into either pristine surfaces or surfaces with high dislocation density and then sputtered with carbon. About 24 hours after indentation the crack opening profile was recorded and the following equation used.

\[
    u = K_{10} \times \frac{E}{1 - \nu^2} \times \sqrt{R s / \pi}
\]

It relates crack tip toughness \( K_{10} \) to the half-opening \( u \), distance to the crack tip, \( x \), and elastic modulus, \( E \) as well as the Poisson’s ratio \( \nu \). In detail, note that the crack is at equilibrium at the time of pop-in, but can be subject to subcritical crack growth in the 24 hours before quantification of the crack opening displacement. Strictly speaking, the crack tip stress intensity factor thus obtained provides a point on the velocity–stress intensity (\( v-K \)) curve, slightly below actual fracture toughness.⁵⁵ However, the ratio of fracture toughness between pristine and dislocation-toughened sample is expected to not be affected.

Electron microscopy

Two samples with high dislocation density at the surface obtained by the dislocation-inducing polishing procedure were glued together to protect the surface layer. A slice was extracted perpendicular to this surface and thinned by conventional polishing and ion milling to afford observation of the gradient of dislocation density from the surface to the center of the sample. The acceleration voltage was set to 1 MeV in STEM mode using the JEOL JEM-1000k RS.

Furthermore, a sample of 2% deformed SrTiO₃ single crystal was cut in a 2° angle to the slip plane and thinned by conventional polishing and ion milling. The acceleration voltage was set to 1 MeV in BF-STEM mode using the JEOL JEM-1000k RS.

Electron channeling contrast imaging (ECCI) was utilized to quantify the density of surface dislocations in the scanning electron microscope (see also Fig. S15, ESI†). High resolution SEM images were acquired using the MIRA3-XMH SEM (TESCAN, Brno, Czech Republic) equipped with a 4-quadrant solid state BSE detector (DEBEN, Woolpit, UK).

From a 2% deformed SrTiO₃ single crystal a slice was cut in a 2° angle to the slip plane so that a FIB-lamella could be prepared with the dislocation line along a [100] direction perpendicular to the lamella thickness. The FIB samples were prepared by FEI Strata DB 235. Using HAADF-STEM atomic resolution images were recorded at 300 kV using an aberration-corrected FEI Titan CubeThemis G2.

Dark-field X-ray microscopy

The experiments were carried out at beamline ID-06 of the European Synchrotron Radiation Facility. A (110) reflection (with the diffraction vector pointing 45° away from the notch and hence parallel to the Burgers vector) at 2θ = 16.86° using a beam with 15.5 keV was selected. The sample was tilted in 2θ to find optimum contrast and rotated around the diffraction vector to tilt the slip planes in the field of view.

For the layer acquisition slices of approximately 400 nm thickness were chosen. A (110) reflection was selected as well, this time normal to the slip plane. The sample was tilted in steps of 0.005° from –0.05° to 0.05° off the diffraction maximum with rotation vectors being [100] and [110] vectors orthogonal to the (110) reflection. For each voxel the mosaicity (the angular position of the intensity maximum in two tilt directions) has been determined using Matlab on the Lichtenberg high performance computer at TU Darmstadt. With a separate scan, where the 2θ angle has been altered as well, the local lattice strain could be quantified in addition to the mosaicity.

Molecular dynamics

Classical molecular dynamics simulations were performed using the LAMMPS simulation software on the Lichtenberg high performance computer at TU Darmstadt. We created a slab-like SrTiO₃ geometry to mimic the experiment on the notched single crystals using periodic boundary conditions along the direction of the notch and along the loading direction. After pre-straining and equilibration compressive stress was applied to the latter direction with a constant engineering strain rate of 1.42 × 10⁸ s⁻¹. The analysis of defects was assisted by post-processing with the software OVITO making use of its dislocation extraction algorithm and atomic strain calculation.⁵⁷,⁵⁸ More details can be found in supplementary 11 (ESI†).

Author contributions

The project was conceived and designed by L. P. and J. R. C. Y., C. D. and H. S. acquired the DFXM data. L. P. and H. S. evaluated the DFXM data. N. L. acquired the HAADF-STEM images under supervision of P. G. A. K. performed the molecular dynamics simulations under supervision of K. A. A. N. acquired the UHVEM images. W. R. provided polycrystalline samples. W. R. and M. H. helped maturing the theoretical and experimental steps. E. P. conducted preliminary experiments. E. B. acquired high-resolution SEM and ECCI images. X. F. and K. D. assisted with indentation data interpretation. All authors discussed the results and commented on the manuscript drafted by L. P.
Conflicts of interest

A related patent has been filed by LP, AK, XF and JR under application number PCT/EP2021/052032.

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