COLD r-PROCESS IN NEUTRINO-DRIVEN WINDS

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ABSTRACT

The r-process in a low temperature environment is explored, in which the neutron emission by photodisintegration does not play a role (cold r-process). A semi-analytic neutrino-driven wind model is utilized for this purpose. The temperature in a supersonically expanding outflow can quickly drop to a few $10^8$ K, where the $(n, \gamma)$-$(\gamma, n)$ equilibrium is never achieved during the heavy r-nuclei synthesis. In addition, the neutron capture competes with the $\beta$-decay owing to the low matter density. Despite such non-standard physical conditions for the cold r-process, a solar-like r-process abundance curve can be reproduced. The cold r-process predicts, however, the low lead production compared to that expected in the traditional r-process conditions, which can be a possible explanation for the low lead abundances found in a couple of r-process-rich Galactic halo stars.

Subject headings: nuclear reactions, nucleosynthesis, abundances — stars: abundances — stars: neutron — supernovae: general

1. INTRODUCTION

It has been generally believed that the high entropy supernova ejecta (neutrino-driven wind) is the likely site for the rapid neutron-capture (r-) process [Woosley & Hoffman 1992; Meyer et al. 1992; Woosley et al. 1994; Takahashi et al. 1994]. In the previous nucleosynthesis calculations related to the neutrino-driven wind scenario, the r-process has been examined in sufficiently high temperature conditions, such that $T_9 \gtrsim 1.0$ (where $T_9$ is the temperature in units of $10^9$ K). This physical condition, as well as the high neutron number density ($N_n > 10^{29}$ cm$^{-3}$), has long been considered as the physical requirements to account for the solar r-process abundance curve [Mathews & Cowan 1990; Kratz et al. 1993]. However, if the neutrino-driven outflow becomes supersonic, the temperature can quickly fall below $T_9 = 1$ [Arcones et al. 2007].

Wanajo et al. (2002) have examined the r-process in such supersonically expanding outflows by introducing the “freezeout temperature” $T_f$ (or $T_{9f}$ in units of $10^9$ K) that mimics the abrupt wind deceleration by the preceding supernova ejecta. In their calculations, the solar r-process curve around the third abundance peak ($A = 195$) was best reproduced with $T_{9f} \approx 1.0$, and the lower $T_{9f}$ (down to 0.6) resulted in forming a lower shifted peak. As shown in Arcones et al. (2007), however, it is quite possible that the wind temperature drops to a few $10^8$ K before deceleration.

In this Letter, the r-process in such a low temperature environment (hereafter “cold r-process”) is explored. A semi-analytic neutrino-driven wind model [Duncan et al. 1986; Qian & Woosley 1996; Cardall & Fuller 1997; Otsuki et al. 2000; Wanajo et al. 2001; Thompson et al. 2001] is used to obtain the thermodynamic histories of outflows ($\S$ 2). Nucleosynthesis calculations in the winds are performed with various $T_{9f}$ including a rather low value that has not been considered in previous works ($\S$ 3). Fundamental behaviors of the cold r-processing are then discussed in some detail. In $\S$ 4, a possible abundance feature in the cold r-process is discussed. Finally, implications of this study are presented ($\S$ 5).

2. NUCLEOSYNTHEIS IN WINDS

The wind trajectories are obtained using the semi-analytic, spherically symmetric, general relativistic model of neutrino-driven winds [Wanajo et al. 2001; 2002]. The rms average neutrino energies are taken to be 10, 20, and 30 MeV, for electron, anti-electron, and the other flavors of neutrinos, respectively. The mass ejection rate at the neutrino sphere $\dot{M}$ is determined so that the wind becomes supersonic through the sonic point.

The neutron star mass is taken to be 1.4 $M_\odot$. The radius of neutrino sphere is assumed to be $R_{\nu} = (R_{\nu0} - R_{\nu1})(L_{\nu}/L_{\nu0}) + R_{\nu1}$ as a function of neutrino luminosity $L_{\nu}$, where $R_{\nu0} = 15$ km, $R_{\nu1} = 10$ km, and $L_{\nu0} = 1 \times 10^{52}$ erg s$^{-1}$. This mimics the early time evolution of $L_{\nu}$ in hydrodynamic simulations [Woosley et al. 1994]. The wind trajectories are calculated for 39 constant $L_{\nu} = (10 - 0.5) \times 10^{51}$ erg s$^{-1}$ with the interval of $0.25 \times 10^{51}$ erg s$^{-1}$. In order to link the series of constant $L_{\nu}$ trajectories to realistic time-evolving winds, $L_{\nu}$ is defined as $L_{\nu}(t_{pb}) = L_{\nu0}(t_{pb}/t_0)^{-1}$, where $t_{pb}$ is the post bounce time and $t_0 = 1.0$ s.

The temperature and density in each wind are set to be constant when $T_3$ decreases to a given freezeout temperature $T_{9f}$ (Fig. 2a), in order to mimic the wind deceleration by the preceding ejecta. In this study, $T_{9f}$ is taken to be 1.3, 1.0, 0.7, 0.4, and 0.1.

The nucleosynthetic yields in each wind are obtained by solving an extensive nuclear reaction network code. The network consists of 6300 species between the proton and neutron drip lines predicted by a recent mass formula (HFB-9, Goriely et al. 2003), all the way from single neutrons and protons up to the $Z = 110$ isotopes (see Wanajo 2006, for more detail). The $\alpha$-decay chains and spontaneous fission processes are taken into account only after the freezeout of all other reactions [Cowan et al. 1999; Wanajo et al. 2002]. Neutron-induced and $\beta$- delayed fissions, as well as the contribution of fission fragments to the lighter nuclei, are neglected.

Each nucleosynthesis calculation is initiated when the temperature decreases to $T_9 = 9$, at which only free nucleons exist. The initial compositions are then given by...
the initial electron fraction $Y_e$ (number of proton per nucleon). In order to mimic the hydrodynamic results (Woosley et al. 1994; Arcones et al. 2007), $Y_e$ is assumed to be $Y_e(L_\nu) = (Y_{e0} - Y_{e1})(L_\nu/L_{\nu0}) + Y_{e1}$. $Y_{e0}$ and $Y_{e1}$ are taken to be 0.50 and 0.15, respectively. The latter is rather smaller than that in hydrodynamic results (e.g., $\sim 0.35$ in Woosley et al. 1994). This extreme assumption is to obtain the heavy $r$-nuclei abundances with a typical neutron star mass ($1.4 M_\odot$) for the current purpose.

3. HOT r-PROCESS VS. COLD r-PROCESS

The nucleosynthetic yields in each $T_{9f}$ case are mass-averaged over the 39 wind trajectories weighted by $M(L_\nu)\Delta t_{pb}$. Figure 1 compares the mass-averaged yields with the solar $r$-process abundances as functions of atomic mass number. We find that, for $T_{9f} = 1.3$ (Fig. 1a), the third-peak abundances shift to the high side from $A = 195$. In addition, the abundance curve is unacceptably jagged compared to the solar $r$-process pattern. For $T_{9f} = 1.0$ (Fig. 1b), the third-peak abundances fit the solar $r$-process pattern quite well. For $T_{9f} = 0.7$ (Fig. 1c), however, the third-peak abundances slightly shift to the low side from $A = 195$.

This can be understood within the classical picture of $r$-process, in which the $(n,\gamma)$-$(\gamma, n)$ equilibrium is justified. That is, for lower $T_{9f}$, the $r$-process path locates at the more neutron-rich side on the nuclide chart. As a result, the freezeout at $N = 126$ takes place at lower $Z$...
Cold r-Process

Fig. 3.— Comparison of the mass-averaged yields (colored lines) with abundances for CS 31082-001 (circles; Hill et al. 2002; Ivanov, S. et al. 2002; Plz& et al. 2004) and the solar r-process curve (black lines; Burris et al. 2008) at the Eu (Z = 63) value, as functions of atomic number. The assigned color in each case is the same as in Figure 1. The vertical scale for the uppermost set is true, and the others are scaled downward for display purposes.

(i.e., lower A). Among the above three cases, $T_{\text{hf}} = 1.0$ can be regarded as a reasonable choice to reproduce the heavy r-process nuclei in the solar system. We find, however, that this interpretation does not hold in the lower $T_{\text{hf}}$ cases. The $T_{\text{hf}} = 0.4$ (Fig. 1d) case reproduces the third-peak abundances even better than the $T_{\text{hf}} = 0.7$ case. Moreover, for $T_{\text{hf}} = 0.1$ (Fig. 1e), the third-peak abundances nicely fit the solar r-process curve. This is a consequence of the cold r-processing as discussed below.

Figure 2 shows some key physical quantities as functions of time ($t = 0$ at $T_9 = 9$) in the $L_\nu = 2 \times 10^{52}$ erg s$^{-1}$ case. The asymptotic entropy per nucleon in this wind is only 92 (in units of the Boltzmann constant). However, the (artificial) low initial $Y_\gamma$ = 0.22 leads to a high neutron-to-seed ratio $Y_n/Y_b = (109)$ at the beginning of the r-process ($T_9 = 2.5$). Here, $Y_n$, and $Y_b$ are the abundances of free neutrons and the heavy nuclei ($Z > 2$), respectively. At $T_9 = 2.5$, the abundance-averaged mass number of the heavy nuclei is 103. This is thus taken to be representative of the third-peak forming winds. On each line in Figure 2, open and filled triangles denote the times when $Y_n/Y_b$ decreases to 80 and 10, respectively. The former and latter approximately correspond to the epochs at which the second ($A = 130$) and third ($A = 195$) peaks form, respectively. Open circles denote the time when $Y_n/Y_b$ decreases to unity, which is referred to as “n-exhaustion.” No heavier nuclei are synthesized beyond this stage, but the rearrangement of the local abundance distribution continues.

The ratios $\tau_{n\gamma}/\tau_{\gamma n}$ and $\tau_\beta/\tau_{\gamma n}$ in each case are shown in Figures 2c and 2d, where $\tau_{n\gamma}$, $\tau_{\gamma n}$, and $\tau_\beta$ are the abundance-averaged mean lifetimes of $(n, \gamma)$, $(\gamma, n)$, and $\beta$-decay for $Z > 2$ nuclei, respectively (see eqs. (3) and (4) in Wanajo et al. 2004). These represent the lifetimes of the dominant species at a given time. The condition $\tau_\beta/\tau_{n\gamma} = 1$ is referred to as “freezeout” (filled circles; Fig. 2). The abundance curve fixes at this time. Note that the classical r-process is characterized by the conditions $\tau_{n\gamma}/\tau_{\gamma n} \approx 1$ and $\tau_\beta/\tau_n \gg 1$.

As can be seen in Figure 2c, the second peak forms at $t = 0.08 - 0.1$ s in all cases, where $\tau_{n\gamma}/\tau_{\gamma n} \approx 1$. This means that the second peak forms under the condition of the $(n, \gamma)$-$(\gamma, n)$ equilibrium. For $T_{\text{hf}} = 1.3$, this condition holds during the whole stage of the r-process. For $T_{\text{hf}} = 1.0$, $\tau_{n\gamma}/\tau_{\gamma n}$ slightly decreases after n-exhaustion and a quasi $(n, \gamma)$-$(\gamma, n)$ equilibrium continues until freezeout. For $T_{\text{hf}} = 0.7$, $\tau_{n\gamma}/\tau_{\gamma n}$ slightly decreases after the second-peak formation and a quasi equilibrium continues by the third-peak formation. In these cases, therefore, the temperature is enough high to maintain the (quasi) $(n, \gamma)$-$(\gamma, n)$ equilibrium during the major r-process phase. Hereafter, the $T_{\text{hf}} = 1.0$ case is taken to be representative of the r-process in a hot temperature environment (hereafter “hot r-process”).

In contrast, in lower $T_{\text{hf}}$ cases, $\tau_{n\gamma}/\tau_{\gamma n}$ quickly drops below unity and the $(n, \gamma)$-$(\gamma, n)$ equilibrium is never achieved after the second-peak formation. This is due to the quickly decreasing $T_9$ and $N_\gamma$, in which the $N_\gamma$-$T_9$ condition abruptly falls off the “waiting point validity boundary” (Cameron et al. 1983; Mathews & Cowan 1990; Goriely & Arnould 1996). The temperature does not play any roles in such an environment, which is thus designated as the cold r-process. Hereafter, the $T_{\text{hf}} = 0.1$ case is taken to be representative of the cold r-process. One may consider that, without photodisintegration, the r-process path approaches the neutron-drip line and the third peak shifts to the rather low side from $A = 195$.

The reason for this misunderstanding can be found in Figure 2d, where the lifetimes of $\beta$-decay and of neutron capture are compared. The hot r-process satisfies the classical r-process condition $\tau_\beta/\tau_n \gg 1$. In the cold r-process, however, $\tau_\beta$ is only a few times larger than $\tau_n$, in which the neutron capture competes with the $\beta$-decay. This is due to the quickly decreasing $N_\gamma$ in the supersonically expanding wind. Consequently, the nucleosynthetic path of the cold r-process is pushed back and locates at a similar position to that of the hot r-process.

This is clearly seen in Figure 2e that shows the r-process path in each case in terms of the neutron separation energy. Here, $S_{n\gamma}/2$ (two-neutron separation energy divided by two) is abundance-averaged for the $Z > 2$ nuclei ($S_a$), which approximately represents the nucleosynthetic path at a given time. That is, $S_a = 0$ is the neutron-drip line, while a higher $S_a$ locates closer to the $\beta$-stability. The path obtained from the $(n, \gamma)$-$(\gamma, n)$ equilibrium condition ($S_a^0$, eq. (3) in Goriely & Arnould 1996) for each is also plotted, which poorly predicts the real path for the cold r-process. The cold r-process takes a significantly higher $S_a$ than $S_a^0$ owing to a push-back by $\beta$-decay. As a result, both the cold and hot r-processes trace similar $S_a$ histories. Notably, the freezeout in the $T_{\text{hf}} = 1.0$ and 0.1 cases takes place at similar $S_a$ values. As a consequence, similar r-process curves appear as can be seen in Figures 1b and 1e. Note that, for $T_{\text{hf}} = 0.1$, freezeout occurs at $T_9 \approx 0.2$. Hence, any $T_{\text{hf}} < 0.2$ cases would result in the identical abundance curve.

4. ABUNDANCE FEATURE IN THE COLD r-PROCESS

1 The animations for $T_{\text{hf}} = 1.0$ and 0.1 are available from http://supernova.astron.s.u-tokyo.ac.jp/~wanajo/research.html.
The abundance differences between the hot and cold r-processes become further small when plotted as functions of atomic number. Figure 3 compares the mass-averaged abundances with the solar r-process curve and the measured elements in the r-process-rich Galactic halo star CS 31082-001. All cases, except for $T_{9f} = 1.3$, are in reasonable agreement with the solar r-process and measured patterns. This may support the robustness of the abundance curves found in the r-process-rich stars. Note that the total mass of the r-process nuclei ($Z \geq 90$) is the same for all cases ($\approx 2.9 \times 10^{-4} M_\odot$), since the seed abundances ($A \sim 100$) are already produced at $T_e \sim 2.5 \times 10^9$ ($> T_{9f}$). The mass fractions of some measurable elements (and $^{195}$Pt) are presented in Table 1, which also shows a small variation between the hot and cold r-processes (up to a factor of two, except for $T_{9f} = 1.3$). These differences are small enough, when considering the uncertainties in the nuclear data as well as in the outflow conditions.

We can see, however, a distinctive feature in the abundance curves around $A = 200 - 230$ (before $\alpha$-decay; black lines in Fig. 1) between the hot and cold r-processes. This is due to their different freezeout histories (Fig. 2e). The hot r-process (red line) follows a low $S_a$ ($\approx 2$ MeV) path at $n$-exhaustion. At this $S_a$ path, a trough at $A \approx 200$ appears in the abundance curve (before $\alpha$-decay, Fig. 1b). This is a consequence that the nuclei at $N \approx 130 - 140$ are predicted to be unstable against neutron capture (see the iso-$S_{1n}/2$ curves in Fig. 6, Wanajo et al. 2004). On the other hand, the cold r-process (blue line) takes a high $S_a$ ($\approx 3$ MeV) path at $n$-exhaustion (Fig. 2e). Therefore, the trough shifts to $A \approx 210$. The trough is further eroded by neutron capture without push-back by photodisintegration. As a consequence, the parent nuclei of Pb ($A = 210 - 231$ and 234; Fig. 1e) result in being significantly deficient. This may lead to a visible difference in the Pb production (Fig. 3 and Table 1), despite the similar Th+U values$^2$.

5. IMPLICATIONS

In this Letter, the r-process in a low temperature environment ($T_{9f} \sim 0.1$; cold r-process) was investigated, which is characterized by the conditions $\tau_{n\gamma}/\tau_{\gamma n} \ll 1$ and $\tau_\beta/\tau_{n\gamma} \gtrsim 1$. Despite the fundamental difference of the cold r-process compared to the traditional (hot) r-process, a solar-like r-process curve can be reproduced quite well. These physical conditions are realized in the supernovally expanding neutrino-driven outflows. In particular, the winds from a low-mass progenitor that has a steep core density gradient easily expand to a large distance (and thus to low $T_{9f}$) before colliding to the preceding supernova ejecta (Arcones et al. 2007). Therefore, the low-mass end of supernova progenitors (e.g., $8 - 12 M_\odot$) may be the most likely site of the cold r-process. The low-mass supernovae have been also suggested to be the r-process site from Galactic chemical evolution studies (Mathews & Cowan 1996; Ishimaru & Wanajo 1999).

Among the six r-process-rich Galactic halo stars currently reported, CS 31082-001 (Plez et al. 2004) and HE 1523-0901 (upper limit, Frebel et al. 2007) appear to have the low Pb abundances compared to the scaled solar r-process curve. The upper limit of Pb for BD +17$^\circ$3248 (Cowan et al. 2002) is still consistent to the scaled solar value. The other three, CS 22892-052 (Sneden et al. 2003), HD 115444 (Westin et al. 2004), and HD 221170 (Ivans et al. 2006) have the measured Pb abundances consistent to the (high) scaled solar value. The variation of the Pb production may be attributed to the different types of (cold and hot) r-processes. The low Pb abundance in CS 31082-001 has in fact a most worrisome aspect, when the U/Th value is applied for the age dating (Plez et al. 2004). This is hardly explained from the classical (or hot) r-process view, in which a low $S_a$ ($\geq 2$ MeV) event is inevitable for the third-peak formation. In this regard, the cold r-process might enable us to consistently treat the Pb, Th, and U abundances for the cosmochronology.

Finally, it is noted that the cold r-process brings us an additional challenge to the theoretical r-process study. In most of previous r-process calculations, the uncertainties in neutron-capture rates have not been considered seriously. This is reasonable for the hot r-process, in which uncertainties even by a factor of ten would not cause a serious problem (see Fig. 2d). In the cold r-process, however, the neutron capture competes with the $\beta$-decay, and thus accurate neutron-capture (as well as $\beta$-decay) rates will be required to predict reliable r-process abundances.

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2 There is a local problem in the odd-even behaviors for $A > 240$ (Fig. 1) when the current nuclear data set is utilized. This leads to an unusual pattern among $^{232}$Th, $^{235}$U, and $^{238}$U, which however does not affect the initial Pb abundance. Therefore, only the sum of Th and U are presented.

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TABLE 1

| $T_{9f}$ | Zr | Ba | Eu | Os | Ir | $^{195}$Pt | Pb | Th+U |
|---------|----|----|----|----|----|-----------|----|------|
| 1.3 | 7.58 | 0.56 | 0.14 | 0.19 | 2.59 | 1.86 | 1.67 | 1.40 |
| 1.0 | 7.97 | 1.89 | 0.20 | 2.04 | 3.24 | 1.69 | 2.06 | 1.27 |
| 0.7 | 8.04 | 1.32 | 0.31 | 2.71 | 3.51 | 1.05 | 1.45 | 1.26 |
| 0.4 | 8.02 | 1.32 | 0.32 | 2.71 | 3.49 | 1.25 | 0.97 | 1.31 |
| 0.1 | 7.97 | 1.32 | 0.36 | 2.34 | 2.97 | 1.58 | 0.92 | 1.25 |
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