A Search for Lensed Lyα Emitters within the Early HETDEX Data Set

Isaac H. Laseter1,2, Steven L. Finkelstein2, Micaela J. Bagley2, Dustin M. Davis5,6,7, Karl Gebhardt2, Gregory R. Zeimann5, Gregory R. Zeimann5,7, and Daniel Farrow7,8

1 Department of Astronomy, University of Wisconsin-Madison, Madison, WI 53706, USA; laseter@wisc.edu
2 Department of Astronomy, The University of Texas at Austin, 2515 Speedway Boulevard, Austin, TX 78712, USA
3 Department of Astronomy & Astrophysics, The Pennsylvania State University, University Park, PA 16802, USA
4 Institute for Gravitation and the Cosmos, The Pennsylvania State University, University Park, PA 16802, USA
5 Hobby Eberly Telescope, University of Texas, Austin, TX, 78712, USA
6 McDonald Observatory, The University of Texas at Austin, Austin, TX 78712, USA
7 Max-Planck-Institut für extraterrestrische Physik, Giessenbachstrasse 1, D-85748 Garching, Germany
8 Universitäts-Sternwarte, Fakultät für Physik, Ludwig-Maximilians-Universität München, Scheinerstr. 1, D-81679 München, Germany

Received 2021 November 12; revised 2022 September 6; accepted 2022 September 11; published 2022 November 15

Abstract

The Hobby–Eberly Telescope Dark Energy Experiment (HETDEX) is a large-volume spectroscopic survey without preselection of sources, searching ~540 deg2 for Lyα emitting galaxies (LAEs) at 1.9 < z < 3.5. Taking advantage of such a wide-volume survey, we perform a pilot study using early HETDEX data to search for lensed Lyα emitters (LAEs). After performing a proof of concept using a previously known lensed LAE covered by HETDEX, we perform a search for previously unknown lensed LAEs in the HETDEX spectroscopic sample. We present a catalog of 26 potential LAEs lensed by foreground, red, non-star-forming galaxies at z ~ 0.4–0.7. We estimate the magnification for each candidate system, finding 12 candidates to be within the strong lensing regime (magnification μ > 2). Follow-up observations of these potential lensed LAEs have the potential to confirm their lensed nature and explore these distant galaxies in more detail.

Unified Astronomy Thesaurus concepts: Gravitational lensing (670); Lyman-alpha galaxies (978)

1. Introduction

Lyα Emitters (LAEs) have been pivotal to the current understanding of galaxy evolution and the epoch of reionization. While LAEs are typically thought of as young, low-mass, star-forming galaxies (Partridge & Peebles 1967), it has been shown that LAEs exhibit a range of properties such as dust content, ages, masses, luminosities, and line profiles (e.g., red line offsets and multicomponent structures with blue wings), leading to a complex and incomplete picture of these galaxies ( Gawiser et al. 2006; Finkelstein et al. 2007, 2008; Lai 2008; Finkelstein et al. 2009; Penterrici et al. 2009; Cowie et al. 2011; Guita et al. 2011; Nilsson & Møller 2011; Atek et al. 2014; Song et al. 2014; De Barros et al. 2017; Oyarzùn et al. 2017; Reddy et al. 2022). An important step in constraining the properties of LAEs is to construct large samples of LAEs spanning a range of luminosities (e.g., Cowie & Hu 1998; Finkelstein et al. 2011; Hill & HETDEX Consortium 2016; Shu et al. 2016; Herenz et al. 2018; Cao et al. 2020).

There have been two primary ways LAE samples have been constructed: (1) narrowband imaging surveys and (2) spectroscopic surveys. Narrowband imaging has the advantage of using optical imagers that allow for large areas of the sky to be probed (~1 deg2; e.g., the Hawaii eROSITA Ecliptic Pole Survey (HEROES; Songaila et al. 2018), the Lyman Alpha Galaxies in the Epoch of Reionization (LAGER; Zheng et al. 2017), the Large Area Lyman Alpha survey (LALA; Rhoads et al. 2001), and the One-hundred-square-degree DECam Imaging in Narrowbands survey (ODIN; Huang et al. 2022). However, narrowband surveys are limited to narrow redshift ranges (e.g., a typical bandwidth is ~Δz = 0.1), and require spectroscopic follow-up to confirm candidates as LAEs. Spectroscopic surveys have been performed through low-resolution slitless spectroscopy (Kurk et al. 2004; Martin et al. 2005), blank-sky slit spectroscopy (Crampton & Lilly 1999; Tran et al. 2004; Rauch et al. 2008; Sawicki et al. 2008; Cassata et al. 2011), and integral-field spectroscopy (Bacon et al. 2010; Adams et al. 2011). Although spectroscopic surveys have the benefit of searching over a larger redshift range due to wider wavelength coverage, the total volume probed is limited due to the limited area of most spectrographs. Overall, a wide-area, spectroscopic survey would be the most efficient way of building large samples of LAEs. While narrowband imaging has historically been more widely used, due to the availability of wide-field imagers, most narrowband searches have been limited to LAEs at LLy* or brighter. Thus, many of these imaging surveys have been unable to fully probe the faint end of the Lyα luminosity function. While recent deep spectroscopic surveys have begun to probe the faint end (e.g., de La Vieuville et al. 2019), the areas observed by such studies are small, and the faintest galaxies are observed at fairly low signal-to-noise ratios, making it difficult to study their physical properties.

One avenue to study fainter LAEs at higher signal-to-noise ratios is to locate LAEs that have been gravitationally lensed by foreground galaxies (galaxy–galaxy lensing; e.g., Warren et al. 1996; Maizy et al. 2009; Shu et al. 2016; de La Vieuville et al. 2019) or by galaxy clusters (cluster lensing; e.g., Atek et al. 2015; Fuller et al. 2020). Galaxy–galaxy lensing surveys, such as the Sloan Lens Advanced Camera for Surveys (SLACS: Bolton et al. 2006), SLACS for the Masses Survey (S4TM; Shu et al. 2015), the Baryon Oscillation Spectroscopic Survey (BOSS) Emission-Line Lens Survey Galaxy-Lyα Emitter Systems (BELLS GALLERY) Survey (Shu et al. 2016), and...
Lensed LAEs in the EBOSS Survey (LESSER; Cao et al. 2020), have the advantage of identifying lensing systems through spectroscopic observations of the foreground galaxy, but are limited in magnification relative to cluster lensing, due to the foreground mass. Cluster lensing surveys, such as the Cluster Lensing And Supernova survey with Hubble (CLASH; Postman et al. 2012), the Hubble Frontier Fields (HFF; Koekemoer et al. 2016; Lotz 2016), and the Reionization Lensing Cluster Survey (RELICS; Coe et al. 2019), have the benefit of pushing the observational limits of high-redshift studies ($z \sim 10$), but typically require deep imaging (e.g., 190 Hubble Space Telescope orbits for RELICS) with spectroscopic follow-up.

Whether it is through galaxy–galaxy lensing or cluster lensing, identifying lensing systems with background LAEs enables fainter LAEs to be studied in detail, due to magnification effects (Stark et al. 2007; Maizy et al. 2009; Ota et al. 2012; Mason et al. 2015; Shu et al. 2015, 2016; Cao et al. 2020). The potential level of “detail” is dependent on the magnification; a higher magnification ($\mu$) factor both increases the apparent brightness and also can result in higher apparent angular resolution. Therefore, it is desirable to isolate lensed LAEs in the strongest lensing regimes. If one targets cluster lenses, strong gravitationally lensed LAEs are more common relative to galaxy–galaxy lensing (e.g., Bina et al. 2016; de La Vieuville et al. 2019; Fuller et al. 2020; Claeyssens et al. 2022), but obtaining the deep imaging and spectroscopic follow-up presents its own obstacles. For galaxy–galaxy lensing systems, strong gravitationally lensed LAEs are rarer, and thus large-volume surveys are required. In this work, we target galaxy–galaxy lensed LAEs, and thus we require a large-volume survey.

The Hobby–Eberly Telescope Dark Energy Experiment (HETDEX; Gebhardt et al. 2021) is a wide-area, integral field spectroscopic survey that will ultimately cover $540 \, \text{deg}^2$. HETDEX covers 3500–5500 Å, and is thus sensitive to Ly$\alpha$ emission at $1.9 < z < 3.5$, providing an excellent opportunity for a wide-area search for rare lenses. Here, we use an early catalog from this in-progress survey to perform a pilot search for LAEs lensed by foreground massive galaxies. For this pilot search, we limit ourselves to red, presumably non-star-forming galaxies, such that any detected emission line should be from a background object, limiting contamination in our survey.

Due to the blue wavelengths observed by the HETDEX Spectrograph (see Section 2.1), detected background emission lines are likely to be Ly$\alpha$. Using the Ly$\alpha$ redshift, the redshift of the lensed galaxy, the angular distance between sources, and lens modeling, the magnification of the system can be calculated. In doing so, favorable systems can be identified for follow-up observations to confirm the presence of LAEs, provide unparalleled details of fainter LAEs, and to aid in ongoing research where fainter LAEs are paramount.

This paper is organized in the following way. In Section 2, we discuss a “proof of concept” of searching for lensed LAEs within HETDEX and how we identified potential foreground lens galaxies to hunt for gravitationally lensed LAEs. In Section 3, we present how we acquired spectra for each potential lensing system and define our procedures for identifying potential background LAEs. In Section 4, we present the procedure of determining the magnification of identified LAE lensing systems. Finally, in Section 5, we summarize our results and discuss future work that could be spurred by this project. We use an $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_m = 0.3$, $\Omega_\Lambda = 0.7$ cosmology throughout the paper.

2. Proof of Concept

2.1. HETDEX

HETDEX is a spectroscopic survey aimed at measuring the Hubble parameter, $H(z)$, and the angular diameter distance, $D_A(z)$, between the redshifts $1.88 < z < 3.52$, the epoch when the majority of the stellar mass in the universe formed (Madau & Dickinson 2014), by observing $\sim 1$ million LAEs. Hunting for LAEs within this redshift range is designed to measure the clustering of galaxies in order to constrain the evolution of the energy density of dark energy. However, the sheer number of LAEs observed through HETDEX provides an extensive data set to explore other frontiers of astronomy, such as galaxy evolution.

HETDEX uses the large Visible Integral-field Replicable Unit Spectrograph (VIRUS; Hill et al. 2021; Indahl et al. 2019), which covers 3500–5500 Å with a resolution of $R \sim 800$ using up to 78 integral field units (IFUs) ($51'' \times 51''$ per IFU), each based on a similar design and each with differences in performance and build. Altogether, the total number of usable fibers (1.5° diameter) with VIRUS is $\sim 34,000$. By performing a spectroscopic survey over $\sim 540 \, \text{deg}^2$, the HETDEX spectroscopic sample size is comparable to the Sloan Digital Sky Survey (SDSS) spectroscopic sample, only at a time 2–3 billion years after the Big Bang. HETDEX is ongoing, with 60% of the survey completed by the end of 2021 (Gebhardt et al. 2021).

The HETDEX reduction algorithm employs an automated emission-line-finding code, extracting fiber spectra to identify emission lines with no positional prior. The vast majority of detections consist of just a single emission line, which is likely to be either Ly$\alpha$ or [O II]. To classify these lines, HETDEX then employs multiple analyses that use all fiber spectra, along with other information such as bandpass continuum estimates, physical size estimates, overlapping neighbor PSFs, etc., from imaging and multiwavelength photometry when available (Leung et al. 2017; Davis et al. 2021; Farrow et al. 2021). The imaging utilized by the HETDEX emission-line-finding code involves a suite of imaging surveys: Hyper Suprime Cam —Dark Energy Experiment (HSC-DEX; HETDEX Specific Survey; $m_{\lim} \sim 25.5$ for a 2″ aperture), the Dark Energy Camera Legacy Survey (DECaLS; $m_{\lim} \sim 24.0$ and $m_{\lim} \sim 23.4–24.0$ for a 2″ aperture), and the HETDEX-Imaging Mosaic taken with the Kitt Peak National Observatory (KPNO) Mayall four-meter telescope in the g-band ($m_{\lim} \sim 23.4$ for a 2″ aperture; observations taken in 2011, 2012, and 2015). HETDEX itself has an $m_{\lim} \sim 24.5–25.0$ for continuum detection when treating the HETDEX spectra as a bandpass. In short, the HETDEX emission-line-finding code utilizes the HETDEX computed mag and every imaging-limited magnitude, which all feed into making a single estimate for the magnitude. This estimated magnitude is then used as a proxy for the continuum, thus enabling a classification/line probability to be determined. Sections 3.2–3.3 explore this procedure in detail.

HETDEX began survey observations in 2017 and has since continued to increase the number and performance of VIRUS units and improve data handling. For the current pilot project, we use HETDEX internal data release 2 (HDR2), which encompasses over $\sim 210$ million spectra, or roughly 35% of the eventual fully completed data set.
2.2. Searching for Known Lensed LAEs

As this work represents the first exploration of the complex HETDEX data set for lensed LAEs, we first performed a “proof-of-concept” study using the positions of 187 potential gravitationally lensed LAEs reported from the BELLs for the GALaxy-Lyα EmitteR sYstems Survey (BELLS GALLERY; Shu et al. 2016). The work by Shu et al. (2016) was chosen for comparison due to their foreground galaxy selection and technique in identifying a lensed LAE candidate. Should any of their lensed sources be covered by HETDEX, we could then use those sources as a test of our ability to discover lensed sources with these data. Shu et al. (2016) utilized data from data release 12 of the Baryon Oscillation Spectroscopic Survey (BOSS), which had a primary goal of delivering redshifts of ~1.5 million luminous red galaxies out to z = 0.7 (Dawson et al. 2013), which represent ideal locations to search for lensed LAEs. Shu et al. (2016) identified potential lensed LAEs by parsing foreground spectra for “rogue” emission lines originating from a background LAE; a procedure similar to the current work discussed in Section 3. The results from Shu et al. (2016) were building off a history of successful SDSS lensing surveys such as SLACS (Bolton et al. 2006) and S4TM (Shu et al. 2015).

To explore which, if any, BELLS GALLERY systems were observed by HETDEX, we searched the HDR2 database for all HETDEX detections within a radius of 360″ of the positions of the known lensed LAEs. The reasoning for such a sizable search radius is to ensure the BELLS GALLERY lensed candidate positions approaching the edge of a HETDEX pointing would be included in this sample. For any matches, we then located and extracted the closest fiber to the positions of the potential lensed LAEs within the HETDEX/VIRUS pointings we returned. We then visually inspected the returned fiber spectra to ensure the respective potential lensed LAEs were encompassed within the fiber coverage.

We found a single BELLS GALLERY LAE candidate that fell on a HETDEX fiber, which is not surprising, given the relatively small fraction of sky HETDEX has covered so far (compared to SDSS), the 1/4.5 filling factor of HETDEX IFUs (the IFUs, even after dithering to cover the interferer gaps, only cover 1/4.5 of the HET focal plane; see Figure 3 of Hill & HETDEX Consortium (2016) and Figure 3 of Gebhardt et al. (2021)), and the low surface density of strong gravitationally lensed systems. We present the extracted HETDEX spectrum for this source (SDSSJ144317.83+510721.0) in Figure 1. According to Shu et al. (2016), the redshift of the foreground source is z = 0.5501 and the redshift of the background source is z = 2.9443 with a Lyα flux of 1.69 ± 0.148 × 10^{-16} erg s^{-1} cm^{-2}. From the extracted HETDEX spectrum, we found a background source redshift of z = 2.9448 with a Lyα flux of 3.60 ± 0.40 × 10^{-16} erg s^{-1} cm^{-2}.

While our flux is higher, a direct comparison between Lyα fluxes reported from Shu et al. (2016) using BOSS and the current work using HETDEX is difficult. BOSS uses single fibers in a plug plate (2″) (Drory et al. 2015), while HETDEX

---

9 The reported error value was not present in the Shu et al. (2016) publication, but obtained through private communication with the authors.
observations consist of three-dither sequences with IFUs, thus collecting more of the total light. In particular, while a single fiber can be aperture-corrected, this typically assumes a point-source profile, while the HETDEX IFU can be sensitive to more extended emission that has been observed in LAEs (e.g., Steidel et al. 2011), which is consistent with our \(~2\times\) higher flux measurement.

The utility of HETDEX for a new lensed search is due to the increased sensitivity of HETDEX. Specifically, although the lensed galaxies BELLs GALLERY finds are similar to what HETDEX can discover, the HETDEX spectroscopic sensitivity is greater, and is thus capable of detecting fainter emission lines down to \(\sim4\times10^{-17}\) erg s\(^{-1}\) cm\(^{-2}\) (Adams et al. 2011; Gebhardt et al. 2021), which corresponds roughly to \(0.5L_{\text{Ly}\alpha}^\text{th}\) at these redshifts (de La Vieuville et al. 2019). For example, the faintest lensed LAE found in Cao et al. (2020), an updated work built off of the original catalog of lensed LAEs from Shu et al. (2016), is \(8.11\times10^{-17}\) erg s\(^{-1}\) cm\(^{-2}\) and was labeled with their lowest confidence interval. The factor-of-two greater sensitivity of HETDEX will allow the detection of intrinsically fainter Ly\(\alpha\) emission, such that lensed LAEs should be more common with HETDEX completed, which we explore in the following sections.

3. Building a Sample of Candidate Lensed LAEs

3.1. Identifying Potential Foreground Lens Galaxies

To search for lensed LAEs in the HETDEX data set, we elected to first identify a population of likely lenses and then explore these galaxies for emission lines. We began constructing a sample of foreground galaxies by obtaining all objects in DR16 from the Sloan Digital Sky Survey (SDSS) with clean photometry within a spectroscopic redshift of \(0.4 \leq z \leq 0.7\). We elected to use SDSS to identify a population of likely lenses, due to the sample size and continuum completion of SDSS (future versions of the HETDEX continuum catalog may make it possible to use HETDEX itself to identify these potential lensed systems). The redshift range was chosen by looking at prior LAE lensing work (Bolton et al. 2006; Brownstein et al. 2012; Shu et al. 2016; Cao et al. 2020), in which all foreground lensing sources were common between \(z \sim 0.4\) and 0.7; moreover, the availability of quality spectra, and thus quality statistics, is greater for the aforementioned redshift range compared with higher-redshift foreground objects that would provide stronger gravitational lensing but limit the overall sample. This redshift constraint yielded \(\sim1.4 \times 10^6\) galaxies.

Prior galaxy–galaxy lensed LAE studies (e.g., Baldry et al. 2004; Cao et al. 2020) targeted red, non-star-forming galaxies for foreground lensing sources, as they are prime environments to hunt for lensed LAEs. There are two central reasons in isolating red, non-star-forming galaxies: (1) these galaxies tend to be more massive, and thus are more efficient at lensing and (2) the spectra of these galaxies typically contain few emission lines relative to star-forming galaxies, which simplifies the search for lensed emission lines overlaid in foreground spectra (see Section 3.3). The current work is acting as a pilot project for HETDEX, and so we are concerned with identifying potential strong lensed LAEs with red, non-star-forming galaxies as the lensing source, thus maximizing the likelihood of a true lensed LAE system through minimal foreground emission lines and strong lensing kernels. A more complete foreground sample, however, would include star-forming galaxies, although their inclusion increases the complexity of magnification estimates discussed in Section 4, due to lensing modeling of spiral galaxies along with a greater entangling of foreground spectra with lensed emission lines. We do not search for potential lensed LAE systems behind star-forming galaxies in the current work.

To isolate red, non-star-forming galaxies from \(\sim1.4 \times 10^6\) redshift selected galaxies, we created a color–magnitude diagram (CMD) of the sample, which we present in Figure 2. We applied color selections of \(1.3 \leq g - r \leq 2.1\) and \(20.8 \leq g \leq 23\) to isolate red, non-star-forming galaxies. The color–magnitude cuts were determined through visual inspection. To select massive red galaxies, we defined the left side of the box to capture the high-density tail end of red galaxies, the bottom side to separate the higher-density region of bluer galaxies (directly below the red dashed line) and QSOs (leftward bottom tail) from the higher-density region of red galaxies, and the upper side to minimize contaminants. From these color–magnitude cuts, we isolated \(\sim130,000\) foreground galaxy candidates to search for within HETDEX coverage as described in Section 2.

The selection of \(g-r\) versus \(r\) would likely be a more appropriate choice here (and for future foreground selection procedures), as the Balmer/4000 Å break occurs over the chosen filters. However, \(g-r\) versus \(g\) suffices in selecting massive galaxies and reducing contaminates. For any red galaxies with active star formation, any emission lines would be flagged through the procedure discussed in Section 3.3.

3.2. Extracting Spectra

With the foreground galaxy sample, the two potential problems from Section 2.2—detections that did not coincide with the exact positions of foreground candidates, and the positions of potential lensed LAEs falling between IFUs—persist, but were handled using a different method than what was stated in Section 2.2. Specifically, when we were proving that HETDEX is capable of detecting known potential lensed LAEs, we possessed the luxury of having the spectra and coordinates of established potential lensed LAEs, and thus were able to exploit the nearest VIRUS fiber to obtain corresponding spectra. With the foreground galaxy sample
we designed, we no longer knew precisely where potential lensed LAEs resided, and thus were not able to immediately extract the result of a specific fiber. Therefore, we retained any foreground galaxy that was covered by HETDEX and employed a more robust method of obtaining spectra for each foreground candidate.

This more powerful, comprehensive method was the utilization of HETDEX’s Emission Line eXplorer (ELiXer; Davis et al. 2021) software, which extracts spectra from the HETDEX HDR2 database. ELiXer is a data visualization, search, and diagnostic tool that combines HETDEX observational data and multiple photometric catalogs to provide a compact, user-friendly representation of emission-line detections to assist the researcher in identifying line-emitting objects and their properties. ELiXer can be used on a desired sky position, where it extracts an assortment of the nearest fibers and weights each fiber based on the distance from the given position and the PSF model, thus resulting in fiber coverage that can detect lensed Lyα emission rather than a single fiber that may or may not be covering the entire foreground galaxy.

In addition to extracting a spectrum centered on the position of the foreground lens galaxy, we used ELiXer to return any spectra within the HETDEX emission-line detection catalog that resided within a 5″ radius of the foreground galaxy’s position. We established a search area around the foreground positions because exclusively searching at foreground positions limited the project to near-perfectly aligned lenses. Extending the search area out to a 5″ radius from the central foreground position allowed us to discover potential lensed LAEs in the strong, intermediate, or weak lensing regimes. Past 5″, the galaxy–galaxy lensing kernel effectively diminishes to zero. Extending our search radius proved to be immensely fruitful and accounted for the majority of our final sample of potential lensed LAEs.

In addition to the added fiber coverage, ELiXer executes its own diagnostics to flag detections that may be spurious or non-astrophysical (bad pixels, meteors, cosmic rays, scattered light, etc.) and returns line identification probabilities based on an aggregate weighting of various information sources (ratios of likelihoods based on equivalent widths, position and flux ratios from other possible emission lines, physical size with assumed redshifts, and more; see Leung et al. 2017; Davis et al. 2021; Farrow et al. 2021; Gebhardt et al. 2021 for more details). The ELiXer success rate in identifying Lyα is ~98% (Davis et al. 2021; Gebhardt et al. 2021), though as we discuss in the following section, we only use these probabilities when considering potential lensed sources >2″ from the lens galaxy (such that the lens continuum does not bias the classification).

3.3. Identification Pipeline/Analysis

To discover potential lensed LAEs, we had to identify Lyα emission within spectra extracted on or close to the selected massive foreground galaxies. To do this, we identified emission lines in our sample by visual inspection. Specifically, out of the ~130,000 SDSS DR16 galaxies selected as lens candidates, 375 were located within regions included in HETDEX HDR 2.1; this makes visual inspection of their extracted spectra feasible. We inspected ELiXer-based spectra extracted both at the position of the potential lens galaxy, as well as at the position of any nearby emission lines identified in the HDR2.1 emission-line catalog (out to a 5″ radius; see Section 3.2).

Although our foreground galaxy sample of red, non-star-forming galaxies was selected to have minimal star-forming emission lines, we could not immediately assume an identified emission line was from a lensed galaxy, as emission lines can originate from processes unrelated to star formation. Therefore, we determined the rest wavelength of each identified emission line by knowing the foreground galaxy’s spectroscopically determined redshift reported from SDSS (see Section 3.4). We then compared the rest wavelength against the full suite of strong and weak emission lines associated with galaxies, AGNs, and Quasi-Stellar Objects (QSOs) between ~700 Å and 10000 Å (e.g., [O III]λ5007, Ne V λ3345.821, Mg II λ2802.705).

The full list of rest wavelengths considered during this process can be found at http://astronomy.nmsu.edu/drewski/tableofemissionlines.html.
the HETDEX emission line matched a known rest wavelength of an emission line at the foreground redshift, it was deemed to originate from the foreground galaxy. Otherwise, we concluded that the emission line was originating from a potentially lensed background galaxy. For example, in Figure 3 the wavelength of the identified emission line is at 4218 Å, which corresponds to a rest wavelength of 2912.4 Å at the foreground redshift $z = 0.4483$. This does not correspond to any wavelengths from our adopted line list, thus likely pointing to a background lensed emission line. We performed this procedure on foreground sources and any neighboring HDR2.1 emission lines identified within 5″ of the foreground galaxy’s position.

For all emission lines, we required the emission line to have a $4.5\sigma$ detection (measured by ELiXer), to attempt to rule out spurious sources. We note that this is similar to cuts used by other early HETDEX projects (e.g., Indahl et al. 2019), and that the majority of our sources have signal-to-noise $>5$. We also visually removed any poor pixel flat subtractions (top left panel in Figure 3), visually verified that the Gaussian fits (top middle panel in Figure 3) were accurate, and visually checked for interlopers in the best available imaging (top right panel in Figure 3). This process yielded nine potential lensed LAEs in the foreground-centered extractions, with an additional 17 lensed LAE candidates found through the neighbor search method described. We present in Figure 4 an example of the neighbor search method.

The overwhelming majority of interlopers within our search were [O II] $\lambda\lambda 3727, 3729$ emitters, which is a common line seen in red galaxies in our foreground redshift search range (Yan et al. 2006; Lemaux et al. 2010). Although the rest wavelength determination step was imperative in uncovering potential lensed LAEs, it did not eliminate the possibility of discovering potential [O II] emitters or any other lensed emission lines. Unfortunately, at $R \sim 800$ (see Section 2.1), the Ly$\alpha$ asymmetry is rarely resolved, so we are not able to use line structure as a line identifier. Therefore, to ensure the
candidate lensed emission lines were potential lensed Lyα emitters, we accessed the aforementioned probabilities calculated by ELiXer regarding the likelihood of the emission line being Lyα. Specifically, ELiXer bases part of the analysis on Leung et al. (2017) to calculate the Lyα probability, with a significant determining factor being the continuum brightness (and thus the line equivalent width).

If a lensed candidate was too close to the foreground galaxy, then the probability of the emission being Lyα was skewed to a lower value, due to the continuum of the foreground galaxy being included in the spectrum, biasing the line equivalent width. Knowing this, if a potential lensed candidate was within ~2″ of the foreground galaxy, we did not immediately eliminate the candidate based on the ELiXer probabilities, but rather relied on our described identification of an emission line with no known associated rest wavelength.

The majority of the positions of our candidates, however, did not fall close enough to the foreground galaxy to skew the probabilities, and thus ELiXer probabilities were still reliable (candidates determined to have foreground continuum contamination are noted in Table 2). Therefore, in addition to the emission lines needing an S/N > 4.5, we aimed for there to be a P(Lyα)/P(\text{QSO}) \geq 3 (a 3:1 ratio in favor of Lyα) for emission lines to be considered confident lensed LAE candidates. This threshold of P(Lyα)/P(\text{QSO}) \geq 3 is explored in Davis et al. (in prep). In short, Davis et al. explore ELiXer’s completeness of LAE identifications versus test data (i.e., recovery rate) under assumed conditions (e.g., P(Lyα)/P(\text{QSO}) \geq 3). ELiXer identifications are compared against ~2500 spec-z sources from various external catalogs, including ~800 sources from the Dark Energy Spectroscopic Instrument (DESI). They find a ~95% recovery rate for the P(Lyα)/P(\text{QSO}) \geq 3 condition assumption. Therefore, our P(Lyα)/P(\text{QSO}) \geq 3 threshold is a good lower limit to help narrow visual inspections and provide confidence to our identifications. Overall, however, the main evidence for potential lensed LAEs is the identification of an emission line inconsistent with the foreground redshift.

We do note that Davis et al. (in prep) used a newer version of the HETDEX emission-line catalog (HDR3) than we used (HDR2; HDR3 was not available at the time of our analysis). However, the data releases are broadly the same, and their differences would not affect the current analysis. These differences lie in the available catalogs (e.g., greater areal coverage in HDR3) and some improvements in the automated ELiXer classifications, but the basic logic is the same. A repeat of the current work with HDR3 might obtain better (deeper) photometric imaging coverage, but the decision of whether an object is a background LAE candidate or not is unlikely to change.

In all, we discovered 26 potential lensed LAEs within the HETDEX data set. Nine LAEs fell on top or near the lens and another 17 were within ~2″–5″ of the foreground lensing galaxy. We present in Table 2 the details of each potential lensed LAE, including a confidence level assigned by the authors based on the quality of the spectrum, S/N, P(Lyα)/P(\text{QSO}) \geq 3, and other returned ELiXer results to indicate which systems are most likely true lensed LAE systems. We present in Figures 3 and 8–31 the foreground spectrum, best available imaging, fiber weights, and the Gaussian fit to the Lyα emission line. The dashed lines in the spectra mark the location of the potential lensed Lyα emission. We present in Figures 5 and 6 the redshift distributions of both the foreground galaxies and the potential lensed LAEs.
Figure 7. Best available imaging for the gravitationally lensed LAE candidates. We present the background lens redshift, magnification determined in Section 4, and the limiting magnitudes of each image, which are reported from the surveys themselves and are survey-wide averages (See Section 2.1). The crosshair of each image focuses on the center of the background LAE candidate position, which is determined from the spectroscopic detection in the HETDEX spectral database found from ELiXer. The values along each axis represent arcseconds away from the central position of the image. The red box represents a ±3″ distance from the center of the image. The overlaid circles represent VIRUS fiber locations, with the colors blue, green, orange, and red representing the fiber weights from strongest to weakest. The imaging was taken directly from ELiXer, which has automatic contrast stretching, i.e., the bright foreground lens causes a poor stretch for identifying fainter regions. Moreover, due to the limited sensitivity of the best available imaging, the background LAE candidates being exceedingly faint, and the foreground object being bright, we do not expect a counterpart to the gravitationally lensed LAE location to be apparent in the current imaging. Nonetheless, the imaging is important to the current work, as the magnification determination (Section 4) requires distances between the foreground lens and the background LAE candidate. With deeper imaging, we expect for a counterpart to the Lyα detection to be discernible. The HSC-r imaging is customized for the HETDEX survey and is not associated with the Subaru Strategic Program.
3.4. SDSS Redshift Confirmation

For the 26 potential lensed LAEs, we confirmed the reported SDSS spectroscopic foreground redshift through visual inspection to ensure the above analysis was valid. If the foreground redshifts were reported incorrectly, then the emission lines we discovered could belong to the foreground galaxy instead of originating from a background, lensed LAE. We analyzed SDSS spectra of the 26 foreground galaxies by identifying emission and absorption lines (primarily Ca K (λ3934.777) and H (λ3969.588) absorption). In all, we found the redshifts to be consistent with SDSS redshifts, thus reinforcing the status of our reported systems as potential lensed LAEs.

Although we found the foreground SDSS redshifts to be correct, we discovered through the redshift vetting process that five of the foreground galaxies in the final lensed LAE candidate systems were identified by SDSS as QSOs. Therefore, unlike the case with ideal foreground candidates and a smaller number of expected emission lines, these QSO foreground galaxies could possess strong and/or less common emission lines. However, as mentioned in Section 3.3, we investigated all known strong and weak emission lines associated with galaxies, AGNs, and QSOs. Therefore, the identified emission lines we present are still likely to be associated with potential lensed LAEs. We present in Table 1 the QSOs in our sample, the rest wavelength of each identified emission line using the foreground redshift, nearby rest wavelength emission lines we vet, and the full width at half maximum (FWHM) of our identified emission lines. In addition to the rest wavelength of the identified emission line not matching any known rest wavelength, the identified emission lines in the QSO foreground spectra have a mean FWHM of ⟨FWHM_QSO⟩ = 6.95 ± 1.26, comparable to the average FWHM of our non-QSO sample of ⟨FWHM_non-QSO⟩ = 6.57 ± 0.34, thus further supporting the identified emission lines as potential lensed LAEs.

4. Magnification Determination

4.1. Magnification

Having a sample of lensed LAE candidates, we wanted to determine which lensing regimes our galaxies fell within, to
identify the most interesting candidates. Specifically, because we searched for lensed LAEs out to 5″ from the foreground galaxies positions, we enabled the detection of strong, intermediate, and weak lensing of LAEs within our sample. To estimate the lensing magnification for our candidates, we followed Mason et al. (2015). Taking our lensing systems as Singular Isothermal Spheres (SIS), the magnification, $\mu$, is given by

$$\mu = \frac{2|\theta|}{|\theta| - \theta_{\text{ER}}}, \quad (1)$$

where $\theta_{\text{ER}}$ is the Einstein radius and $\theta$ is the image distance between the foreground galaxy and lensed source (Mason et al. 2015). The SIS assumption ignores neighboring galaxies that may potentially affect the magnification of the background source. For example, in Figure 7 there are systems where nearby galaxies are present that could modify the magnification strength; however, these galaxies are unlikely to play a significant role in magnification, due their fainter fluxes and thus likely lower masses relative to the primary foreground galaxy. Ultimately, under the SIS assumption, these proximate galaxies are ignored.

The $\mu$ determination yields what lensing regime each lensed LAE candidate falls within. Specifically, $\mu > 2$ is strong lensing, $1.4 < \mu < 2$ is intermediate lensing, and $\mu < 1.4$ is weak lensing. We determined the Einstein radius from

$$\theta_{\text{ER}}(\sigma, z) = 4\pi D_{ls} D_{s}^2 \frac{\alpha}{c}, \quad (2)$$

where $D_{ls}$ is the angular diameter distance between the lens and source, $D_s$ is the angular diameter distance between the observer to the source, $\sigma$ is the velocity dispersion of the lensed LAE candidate, and $c$ is the speed of light (Mason et al. 2015). For $\sigma$, we utilized the Mason et al. (2015) correlation between velocity dispersion, redshift, and apparent magnitude of the foreground galaxies. We also utilized the SDSS $i'$ band for the magnitude dependence in the velocity dispersion relation from Mason et al. (2015).

We accounted for the uncertainties in the Mason et al. (2015) velocity dispersion—magnitude estimates and error induced by the PSF weighting of the VIRUS fibers ($\sim 0''5$; see Gebhardt et al. (2021) for more details) by employing a Monte Carlo error propagation technique. We evaluated Equation (1) 10,000 times for each lensing candidate using values drawn randomly from normal distributions centered on the velocity dispersion error from Mason et al. (2015). Specifically, from Mason et al. (2015):

$$\log(\sigma) = -0.1 \times m + a \times \log(1 + z) + b, \quad (3)$$

where $\sigma$ is the velocity dispersion, $m$ is the $i$-band magnitude, and $a$ and $b$ are constants. For

$z < 0.5$: $a = 2.26 \pm 0.79, b = 4.08 \pm 0.12, \quad (4)$

for

$0.5 < z < 1.0$: $a = 0.93 \pm 0.13, b = 4.20 \pm 0.03, \quad (5)$

and for

$z > 1.0$: $a = 1.02 \pm 0.15, b = 4.12 \pm 0.05. \quad (6)$

The standard deviation of each 10,000 runs per lensing candidate represents the 1σ error for the magnification determination, and the median value represents $\mu$. For a comprehensive overview of the Monte Carlo error propagation technique, please refer to Andrae (2010).

In total, we have 12 candidate strong lensing systems, seven intermediate lensing systems, and seven weak lensing systems in our sample. Table 2 lists the magnification for each candidate, $z_{\text{source}}, z_{\text{ls}}, S/N$, positions, Ly$\alpha$ flux, LAE probability, and a confidence level, which was chosen by the authors based on the quality of spectra, $S/N$, and P(LAE)/P(O II). Figures 5 and 6 present the distribution of $\mu$ against corresponding redshift for foreground galaxies and background lensed LAE candidates, respectively.

Follow-up observations are necessary to confirm the background galaxies as LAEs. Therefore, it was warranted to constrain the magnification of each system and establish a confidence level in order to note the lensing systems of most interest. Overall, the candidates with a high confidence level and with a magnification of $\mu \geq 2$ are the best targets for follow-up observations.

We present in Figure 7 the best available imaging, which we obtain using ELiXer, for the current potential lensed LAE catalog. Although the lensed LAEs are not obvious in the imaging, this is not unexpected, due to the limiting magnitude of the current imaging, which is given for each candidate system in Figure 7, being shallow relative to the expected magnitude of a faint, background LAE. Nonetheless, the available imaging will aid in future studies spurred by the current catalog. Specifically, having the best available imaging, the magnification of each system, and the confidence level of each emission creates a solid foundation for future observations and work.

4.2. Expected Number of LAEs

In an effort to explore the validity of our sources as candidate lenses, we compare our observed number of 26 potential lenses to two predicted values. For both predictions, we compare their observed surface density to that in the overall internal HETDEX emission-line catalog, which, to our chosen signal-to-noise and Ly$\alpha$ probability cuts ($S/N \geq 4.5$ and P(LAE)/P(O II) $\geq 3$), has a surface density of 3.4 LAEs arcmin$^{-2}$. We caution that this should be viewed as a lower limit for the expected true surface density of lensed sources, as the lensed sources are intrinsically fainter than unlensed HETDEX sources, and thus will have higher intrinsic volume densities due to the shape of the Ly$\alpha$ luminosity function. For our lensing search, we found 26 candidate lenses over an image-plane search area with a radius of 5″ around 375 candidate lens systems with HETDEX spectra, resulting in a surface density of $\sim 3.2$ LAEs arcmin$^{-2}$. Thus, our search around potential lens systems yields approximately the expected source density, which is positive evidence against a significant spurious emission-line fraction in our sample (which is expected, as we specifically targeted galaxies expected to have minimal emission-line features).

As a second sanity check, we compare our observations to the predicted number of lensed galaxies. This requires us to a priori assume the angular separation between the lens and the source in the source plane, denoted as $\beta$. To decide on this distribution, we tested $\beta$ distributions using the sample of 375 searched lens galaxies, in each case calculating the observed
source-lens separation $\theta$ using the known lens redshift, and a randomly drawn source lens redshift in the HETDEX redshift range of 1.9–3.5. We found that assuming a flat random distribution of $\beta = 0''–2''$ resulted in a $\theta$ distribution in agreement with that observed for our lensed galaxy sample, with a median of $\theta \approx 4''$, and tails to both lower and higher values. A K-S test comparing these created distributions to our observed distributions gives a $\geq 50\%$ probability that they were drawn from the same distribution.

Using this $\beta$ distribution, we then ran 1000 Monte Carlo simulations. In each simulation, we considered whether a given potential lens galaxy would have a HETDEX LAE behind it, using the HETDEX surface density ($3.4\, \text{LAEs arcmin}^{-2}$) and a search area with a radius of $3''$ (e.g., the maximum of our $\beta$ distribution). This calculation implies that each lens system has a 2.6% chance of having a true background LAE in the HETDEX redshift range. During each Monte Carlo simulation, we thus randomly assigned 2.6% of the lens systems to have a background HETDEX LAE, and calculated the magnification. We then further calculated, for each simulation, the number of weak, intermediate, and strongly lensed systems. Using the median and standard deviation of these numbers across all 1000 simulations, we predict that we should have discovered 1 $\pm 0.2$ weak, 1 $\pm 1$ intermediate, and 7 $\pm 2.7$ strongly lensed galaxies. Overall, this expectation of nine lensed galaxies is less than our sample size of 26 potential lenses, highlighting the need for follow-up deep and high-resolution imaging observations to confirm the lensed nature of these sources.

We note that our simple calculations are difficult for a variety of reasons, including the impact of subjective visual inspections during our candidate lensed galaxy selection process (where we implemented several qualitative cuts to arrive at a robust list of emission lines, which are not encapsulated in the internal HETDEX emission-line catalog surface density), the impact of lensing distortion of the search volume (for the image-plane prediction), and also that the area within our search radius to where we are sensitive to emission lines is likely less than the full area, due to confusion with the light (and associated noise) from the lens galaxy itself. We conclude that follow-up observations of our candidate lens systems, ideally high-resolution imaging with, e.g., the Hubble Space Telescope, are needed to confirm the validity of these systems.

5. Summary/Future

We have discovered 26 potential gravitationally lensed LAEs within the HETDEX data set (Figures 1, 3, 8-31). We isolated these potential lensing systems by visually inspecting fiber-weighted spectra extracted with ELiXer and utilizing emission-line probabilities determined from ELiXer. In addition to finding the potential lensed LAE systems, we determined the magnification for each potential lensed LAE system. We found 12 potential LAEs within the strong lensing regime, seven within the intermediate regime, and seven within the weak lensing regime. Based on the visual inspection of the spectra, magnification, emission-line probabilities, $S/N$, and emission-line fits, we assigned a confidence level of LAE likelihood to each candidate, which we present in Table 2.

HETDEX is only $\sim 35\%$ complete. Therefore, as HETDEX progresses, so will the number of potential gravitationally lensed LAEs observed by HETDEX. For this project, we set out not only to provide a list of potential gravitationally lensed LAEs, but also to establish a foundation for an analogous project to be launched once HETDEX is complete.

The lensed LAE candidates presented in this paper require observational follow-up to confirm the lensing status. If confirmed, the science that can be performed on the background LAEs is wide-ranging. For research concerned with the epoch of reionization, the added observational detail and number of lensed LAEs enables stronger constraints on the relative contribution of star-forming galaxies to cosmic reionization. For research concerned with galaxy evolution, observing lensed LAEs that would be too faint to observe if they had not been gravitationally lensed enables improvements on luminosity functions such as constraining the faint-end slope, which remains unconstrained. Moreover, lensed LAEs give a more detailed image of Milky Way progenitors. For example, Shu et al. (2016) used strongly lensed LAEs to obtain the morphology of the LAEs down to $\sim 100$ pc regions. In addition to the morphology of LAEs, the line profiles of Ly$\alpha$ emission are still not fully understood (Yamada et al. 2012). Specifically, the origin of Ly$\alpha$ emission does not have a dominant identified source and the process of Ly$\alpha$ photon escape from the galaxies is labyrinthine (Yamada et al. 2012), thus leading to varying Ly$\alpha$ profiles. Possessing detailed observations on the candidates identified in this paper can provide insight for the diverse theoretical models of Ly$\alpha$ escape and sources.

In all, the work presented here lays the foundation for subsequent work to be performed once HETDEX is completed, identifies potential gravitationally lensed LAE systems, and determines the magnification for each lensing system.

We thank Sangeeta Malhotra for stimulating conversations that led to this work, and the staff at McDonald Observatory for their tremendous effort to build this new VIRUS instrument. HETDEX is led by the University of Texas at Austin McDonald Observatory and Department of Astronomy with participation from the Max-Planck-Institut für Extraterrestrische Physik (MPE), Leibniz-Institut fi die Astrophysik Potsdam (AIP), Texas A&M University, Pennsylvania State University, Institut für Astrophysik Göttingen, The University of Oxford, Max-Planck-Institut für Astrophysik (MPA), The University of Tokyo, and Missouri University of Science and Technology. In addition to Institutional support, HETDEX is funded by the National Science Foundation (grant AST-0926815), the State of Texas, the US Air Force (AFRL FA9451-04-2- 0355), and generous support from private individuals and foundations. The observations were obtained with the Hobby–Eberly Telescope (HET), which is a joint project of the University of Texas at Austin, the Pennsylvania State University, Ludwig-Maximilians-Universität München, and Georg-August-Universität Göttingen. The HET is named in honor of its principal benefactors, William P. Hobby and Robert E. Eberly. The authors acknowledge the Texas Advanced Computing Center (TACC) at The University of Texas at Austin for providing high-performance computing, visualization, and storage resources that have contributed to the research results reported within this paper.

URL: http://www.tacc.utexas.edu The Institute for Gravitation and the Cosmos is supported by the Eberly College of Science and the Office of the Senior Vice President for Research at the Pennsylvania State University. We gratefully thank the University of Texas, the HETDEX collaboration,
the University of Texas High Z Group, and The John W. Cox Endowment for Advanced Studies in Astronomy for their generosity. Isaac Laseter and Steven Finkelstein acknowledge support from the National Science Foundation, through grant AST-1908817.

Appendix

Following the layout presented in Figure 1, we present in Figures 8–31 the remaining potential gravitationally lensed LAEs in our sample.

Figure 8. 20181225v008-9900000001. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$.

Figure 9. 20181115v016-9900000004. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$. 
Figure 10. 20190325v015-9900150001. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$.

Figure 11. 20190630v013-9900030001. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$. 
Figure 12. 20191217v011-9900060004. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Lyα.

Figure 13. 20190306v014-9900010001. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Lyα.
Figure 14. 20181204v030-9900010004. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$.

Figure 15. 20170923v017-9900050003. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$. 
Figure 16. 20190504v019-9900150006. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$.

Figure 17. 20190316v023-9900090004. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$. 
Figure 18. 20191029v020-9900140002. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$.

Figure 19. 20181108v021-9900080002. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$. 
Figure 20. 20180912v018-9900070002. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Lyα.

Figure 21. 20190429v016-9900140004. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Lyα.
Figure 22. 20180516v009-9900100002. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of $\text{Ly} \alpha$.

Figure 23. 20190901v019-9900190001. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of $\text{Ly} \alpha$. 
Figure 24. 20171120v006-9900050002. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$.

Figure 25. 20180411v012-9900160001. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$. 
Figure 26. 20190403v022-9900000002. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Lyα.

Figure 27. 20180913v018-9900100003. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Lyα.
Figure 28. 20200129v020-9900060001. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$.

Figure 29. 20181205v014-9900080003. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$. 
Figure 30. 20190808v018-9900040003. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$.

Figure 31. 20181115v016-9900070005. Top Left: Two best VIRUS fibers, pixel flats, smoothed VIRUS fibers, and weighted sum of fibers. Top Middle: Gaussian fit to emission line. Top Right: Best available imaging on location of lensed LAE candidate. Bottom: Full spectrum of lensed LAE candidate. The yellow box with a dashed line denotes the location of Ly$\alpha$. 
Finkelstein, S. L., Rhoads, J. E., Malhotra, S., Pirzkal, N., & Wang, J. 2007, ApJ, 660, 1023
Fuller, S., Lemaux, B. C., Bradač, M., et al. 2020, ApJ, 896, 156
Gawiser, E., van Dokkum, P. G., Gronwall, C., et al. 2006, ApJL, 642, L13
Gebhardt, K., Mentuch Cooper, E., Ciardullo, R., et al. 2021, ApJ, 923, 217
Guaita, L., Acquaviva, V., Padilla, N., et al. 2011, ApJ, 733, 114
Herenz, E. C., Wisotzki, L., Saust, R., et al. 2018, yCat, J/A+A/621/A107
Hill, G. J. & HETDEX Consortium 2016, in ASP Conf. Ser. 507, Multi-Object Spectroscopy in the Next Decade: Big Questions, Large Surveys, and Wide Fields, ed. I. Skillen, M. Balcells, & S. Trager (San Francisco, CA: ASP), 393
Hill, G. J., Lee, H., MacQueen, P. J., et al. 2021, AJ, 162, 1
Huang, Y., Lee, K.-S., Cucciati, O., et al. 2022, arXiv:2206.07101
Indahl, B., Zeimann, G., Hill, G. J., et al. 2019, ApJ, 883, 114
Koekenkoer, A. M., Mack, J., Lotz, J. M., et al. 2016, AAS Meeting Abstracts, 228, 315.02
Kurk, J. D., Cimatti, A., di Serego Alighieri, S., et al. 2004, A&A, 422, L13
Lai, K. Y. Y. 2008, PhD thesis, Harvard Univ.
Lemaux, B. C., Lubin, L. M., Shapley, A., et al. 2010, ApJ, 716, 970
Leung, A. S., Acquaviva, V., Gawiser, E., et al. 2017, ApJ, 843, 130
Lotz, J. 2016, IAUFM, 29B, 751
Madau, P., & Dickinson, M. 2014, ARA&A, 52, 415
Maiz, A., Richard, J., De Leo, M. A., Pelló, R., & Kneib, J. P. 2009, A&A, 509, A105
Martin, D. C., Fanson, J., Schiminovich, D., et al. 2005, ApJL, 619, L1
Mason, C. A., Treu, T., Schmidt, K. B., et al. 2015, ApJ, 805, 79
Nilsson, K. K., & Møller, P. 2011, A&A, 527, L7
Ota, K., Richardson, J., Iye, M., et al. 2012, MNRAS, 423, 2829
Oyarzún, G. A., Blanc, G. A., González, V., Mateo, M., & Bailey, J. I. I. 2017, ApJ, 843, 133
Partridge, R. B., & Peebles, P. J. E. 1967, ApJ, 147, 868
Pentericci, L., Grazian, A., Fontana, A., et al. 2009, A&A, 494, 553
Postman, M., Cimatti, A., Madau, P., et al. 2012, ApJ, 769, 25
Rauch, M., Haehnelt, M., Bunker, A., et al. 2008, ApJ, 681, 856
Reddy, N. A., Topping, M. W., Shapley, A. E., et al. 2022, ApJ, 926, 31
Rhoads, J. E., Malhotra, S., Dey, A., et al. 2001, in ASP Conf. Ser. 232, The New Era of Wide Field Astronomy (San Francisco, CA: ASP)
Savicki, M., Lemaux, B. C., Guhathakurta, P., et al. 2008, ApJ, 687, 884
Shu, Y., Bolton, A. S., Brownstein, J. R., et al. 2015, ApJ, 803, 71
Shu, Y., Bolton, A. S., Mao, S., et al. 2016, ApJ, 833, 264
Song, M., Finkelstein, S. L., Gebhardt, K., et al. 2014, ApJ, 791, 3
Songaila, A., Hu, E. M., Barger, A. J., et al. 2018, ApJ, 859, 91
Stark, D. P., Ellis, R. S., et al. 2007, ApJ, 663, 10
Steidel, C. C., Bouwens, R., Shapley, A. E., et al. 2011, ApJ, 736, 160
Tran, K.-V. H., Lilly, S. J., Crampton, D., & Brodfink, M. 2004, ApJL, 612, L89
Warren, S. J., Hewett, P. C., Lewis, G. F., et al. 1996, MNRAS, 278, 139
Yamada, T., Matsuda, Y., Kousai, K., et al. 2012, ApJ, 751, 29
Yan, R., Newman, J. A., Faber, S. M., et al. 2006, ApJ, 648, 281
Zheng, Z.-Y., Wang, J., Rhoads, J., et al. 2017, ApJL, 842, L22