Atomic carbon, nitrogen, and oxygen forbidden emission lines in the water-poor comet C/2016 R2 (Pan-STARRS)

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\textbf{ABSTRACT}

\textbf{Context.} The N\textsubscript{2} and CO-rich and water-depleted comet C/2016 R2 (Pan-STARRS) (hereafter ‘C/2016 R2’) is a unique comet for detailed spectroscopic analysis.

\textbf{Aims.} We aim to explore the associated photochemistry of parent species, which produces different metastable states and forbidden emissions, in this cometary coma of peculiar composition.

\textbf{Methods.} We re-analyzed the high-resolution spectra of comet C/2016 R2, which were obtained in February 2018, using the UVES spectrograph of the European Southern Observatory (ESO) Very Large Telescope (VLT). Various forbidden atomic emission lines of [CI], [NI], and [OI] were observed in the optical spectrum of this comet when it was at 2.8 au from the Sun. The observed forbidden emission intensity ratios are studied in the framework of a couple-chemistry emission model.

\textbf{Results.} The model calculations show that CO\textsubscript{2} is the major source of both atomic oxygen green and red-doublet emissions in the coma of C/2016 R2 (while for most comets it is generally H\textsubscript{2}O), whereas, CO and N\textsubscript{2} govern the atomic carbon and nitrogen emissions, respectively. Our modelled oxygen green to red-doublet and carbon to nitrogen emission ratios are higher by a factor of 3, when compared to the observations. These discrepancies can be due to uncertainties associated with photon cross sections or unknown production/loss sources. Our modelled oxygen green to red-doublet emission ratio is close to the observations, when we consider an O\textsubscript{2} abundance with a production rate of 30% relative to the CO production rate. We constrained the mean photodissociation yield of CO producing C(1S) as about 1%, a quantity which has not been measured in the laboratory. The collisional quenching is not a significant loss process for N(2) though its radiative lifetime is significant (~10 hrs). Hence, the observed [NI] doublet-emission ratio ([NI] 5198/5200) of 1.22, which is smaller than the terrestrial measurement by a factor 1.4, is mainly due to the characteristic radiative decay of N(2).

\textbf{Keywords.} Comets: individual: C/2016 R2 (PanSTARRS), Techniques: spectroscopic, molecular processes, forbidden lines

1. Introduction

Comets are considered as pristine objects and can provide clues about the initial formation conditions of the Solar System. These objects have undergone little alteration since birth because they spent most of their lifetime in remote reservoirs far away from the Sun. Various successive ground and spacecraft observations have confirmed that comets are primarily composed of water ice amalgamated with organic molecules and refractory dust. When a comet reaches the vicinity of the Sun, solar radiation sublimes the ices present in the nucleus and produces a gaseous envelope called a cometary coma. The interaction of the solar radiation with the coma drives a plethora of chemical reactions and leads to various spectral emissions from cometary species (Feldman \textit{et al.} 2004, Rodgers \textit{et al.} 2004).

Remote spectroscopic observations are the primary tool to reveal the parent species distribution in the cometary coma and also to assess the global composition of comets (Feldman \textit{et al.} 2004). Among the various emissions observed in cometary spectra, the emissions due to optically forbidden electronic transitions of metastable species have been used as direct tracers of cometary parent molecules. The formation of these metastable species occurs mainly due to the dissociative excitation of parent species in the coma. Solar resonance fluorescence is an insignificant excitation mechanism in populating these excited states (Festou & Feldman 1981). Hence, the radiative emissions of these species have been used as a proxy to trace and also to quantify the sublimation rates of parent species in comets (Delsemme \& Combi 1976, Delsemme \& Combi 1979, Fink \& Johnson 1984, Magee-Sauer \textit{et al.} 1990, Schulz \textit{et al.} 1992, Morgensthaler \textit{et al.} 2001, Furusho \textit{et al.} 2006, McKay \textit{et al.} 2012a,b, McKay \textit{et al.} 2019, Decock \textit{et al.} 2013, 2015).

In spite of being the predominant species in the coma of most comets, water cannot be observed directly in the visible region due to the lack of electronic transitions. Hence, atomic oxygen forbidden emissions (red-doublet at 6300 & 6364 Å, and green at 5577 Å wavelengths), which are produced during the photodissociation of water, have been regularly used to quantify the H\textsubscript{2}O sublimation rate of the nucleus (see Bhardwaj \& Raghuram 2012 for more details on various atomic oxygen emission observations in comets). Similarly, the atomic carbon 1931 Å emission line, which is mainly due to the resonance fluorescence of the C(1D) state, has been used as a diagnostic tool to derive the CO abundance in several comets (Feldman \& Bruc 1976, Smith \textit{et al.} 1980, Feldman \textit{et al.} 1980, 1997, Tozzi \textit{et al.} 1998, Oliversen \textit{et al.} 2002) observed C(1D) radiative decay emissions at wavelengths 9850 and 9824 Å in comet C/1995 O1 Hale-Bopp and the observed emission intensity has been used to constrain the CO production rate. Even though Singh \textit{et al.} (1991) predicted atomic nitrogen forbidden emissions at wavelengths 5200 and 5198 Å in comets, these emissions were never observed be-
fore. Opitom et al. (2019) recently observed comet C/2016 R2 and reported the first-ever atomic nitrogen forbidden emissions.

Several works have discussed the photochemistry of metastable states in water-dominated cometary comae (Festou & Feldman 1981; Bhardwaj & Haider 2002; Bhardwaj 1999; Saxena et al. 2002; Bhardwaj & Raghuram 2012; Raghuram & Bhardwaj 2013, 2014; Decock et al. 2015; Raghuram et al. 2016; Cessateur et al. 2016a,b). The observed atomic oxygen green to red-doublet emission intensity ratio (hereafter [OI] G/R ratio) has been used as a proxy to confirm water as a dominant source of these emission lines in comets. However, the Bhardwaj & Raghuram (2012) modelling studies of atomic oxygen emission lines in comet C/1996 B2 (Hyakutake) have shown that the [OI] G/R ratio is not a constant in the cometary coma and varies as a function of nucleocentric distance. These studies also suggested that the [OI] G/R ratio is not a proper tool to confirm that water is the dominant source of atomic oxygen forbidden emission lines. Decock et al. (2015) observed atomic oxygen emissions in different comets and found that the [OI] G/R ratio varies as a function of the nucleocentric distance. By studying the photochemistry of these emission lines, the observed [OI] G/R ratio has been used to derive CO₂ abundances on different comets. Raghuram & Bhardwaj (2013) have studied the photochemistry of these lines in a very active comet viz., C/1995 O1 Hale-Bopp, and have shown that CO₂ is also a potential candidate for the formation of O(S) in the cometary coma when its presence is substantial (more than 5% with respect to H₂O). This work has also shown that photodissociation of CO₂ leads to the formation of O(S) with higher excess velocities compared to the photodissociation of H₂O, which could be a reason for the observation of the larger width of green lines compared to the red-doublet emissions. By considering the photochemical production and loss pathways of major species, the modelling studies of Bhardwaj & Raghuram (2012), Raghuram & Bhardwaj (2013), and Raghuram & Bhardwaj (2014) explained the observed [OI] G/R ratio in different comets observed at various heliocentric distances. These studies also constrained the photodissociation yield of water producing O(S) at Lyman-α wavelength as about 1% of the total absorption cross section. After detection of molecular oxygen in comets 67P-Churyumov-Gerasimenko (Bieler et al. 2015; Altwegg et al. 2019) and 1P/Halley (Rubin et al. 2015), the photochemical model developed by Cessateur et al. (2016a) has shown that not considering the role of O₂ in the photochemistry of [OI] emissions leads to an underestimation of the CO₂ abundance in comets.

All the previously mentioned works aimed to study the photochemistry of forbidden emission lines in a water-dominated cometary coma. The recent spectroscopic observations of C/2016 R2, which were made when the comet was around 2.8 au from the Sun, have shown that this comet has a peculiar composition even compared to other comets observed at large heliocentric distances (Cochran & McKay 2018; Biver et al. 2018; de Val-Borro et al. 2018; Wierzchos & Womack 2018; Opitom et al. 2019; McKay et al. 2019). Cometary optical spectra are usually dominated by various resonance fluorescence lines of radicals such as OH, NH, CN, C₂, and NH₂. However, the observations of C/2016 R2 have shown that its coma is rich in N₂ and CO and depleted of H₂O, HCN, and C₂, which is unusual and makes this comet a unique case among the comets observed so far (Biver et al. 2018; Opitom et al. 2019; McKay et al. 2019). Opitom et al. (2019) have observed several atomic oxygen (5577, 6300, & 6364 Å), carbon (8727, 9824, & 9850 Å) and nitrogen (5197 & 5200 Å) forbidden emission lines in C/2016 R2. Fig. 1 shows the electronic transitions of these forbidden emission lines. Since these emissions originate from metastable states, which have long radiative lifetimes (≥0.5 s), the collisional quenching in the inner coma should be accounted for while determining the emission intensities. Moreover, the formation and destruction of these atomic metastable states are associated to several parent species present in the coma. The main production pathways of metastable states due to the interaction of solar ultraviolet photons (hν) and suprathermal electrons (e⁻ph) with major parent species are:

\[ h\nu + e^{-}_{ph} + H_2O \rightarrow O(1S, \ ^1D) + H_2 \]
\[ h\nu + e^{-}_{ph} + CO_2 \rightarrow C(1S, \ ^1D) + O(1S, \ ^1D) + O \]
\[ h\nu + e^{-}_{ph} + CO \rightarrow C(1S, \ ^1D) + O(1S, \ ^1D) \]
\[ h\nu + e^{-}_{ph} + N_2 \rightarrow N(1D, \ ^2P) + N \]

The detection of these various forbidden emissions in a water-poor comet (<1% relative to total gas production rate) has motivated us to study the photochemistry of the atomic carbon, oxygen and nitrogen metastable states and also their emission processes in C/2016 R2. We have modelled all these emission lines in the framework of earlier developed coupled-chemistry emission models. The observations of this comet are described in Section 2. The inputs required to model the observed emission ratios and calculations are described in Section 3. The results of model calculations are presented in Section 4 followed by a discussion in Section 5. We summarise and conclude the present work in Section 6.

2. Observations

Observations of C/2016 R2 were carried out on 2018 February 11-16 with the Ultraviolet-Visual Echelle Spectrograph (UVES) mounted on the 8.2m UT2 telescope of the European Southern Observatory Very Large Telescope (VLT). The slit width of 0.44″ provides a resolving power R ≈ 80000. The seeing was 0.9″ during the observations of the [OI], [NI] lines (UVES setting 390+580) and 1.0″ during the observations of the [CI] lines (UVES setting 437+860). More details about the observations and data reductions are given in Opitom et al. (2019).

Surface brightness measurements of the [OI], [CI] and [NI] lines were carried out on the two-dimensional spectra, cutting the slit in chunks as done in Decock et al. (2015) and illustrated in Fig. 2. The size of one pixel projected onto the comet is 310 km, neglecting the differences (smaller than 5%) between the dates of observations and the different settings. The full slit thus extends over ∼2 × 10⁴ km projected on the comet. The nights Feb. 13 and Feb. 14 were affected by thin clouds while the other nights were clear. To account for cloud extinction, the fluxes are multiplied by 1.10 and 1.05 for the nights Feb. 13 and Feb. 14, respectively. These factors were estimated by assuming that the full-slit fluxes in the bright lines are identical on Feb. 11, Feb. 13, and Feb. 14. The contamination by C₂ band emission, which generally can affect the [OI] 5577 observation (Decock et al. 2015), is negligible in this comet due to the very small amount of C₂ in the coma of this comet (Opitom et al. 2019). The measurements obtained on the different nights were averaged. The extractions done on each side of the slit in a given range of nucleocentric distances were also averaged.

The measured surface brightness of the different lines is presented in Table 1 in relative flux units, as a function of the nucleocentric projected distance. Errors were computed from propagated photon noise and from the dispersion of the night-to-night measurements, the largest of the two values being reported in
The observed line intensity ratios of interest are given in Table 2. We find that at high nucleocentric projected distances (>102 km), the observed [OI] G/R ratio in C/2016 R2 does not match the value of 0.05, which is usually measured in water-dominated comets (Decock et al. 2015). In this Table we also present the observed emission ratio of [CI] 8727 Å to (9824+9850) (hereafter [CI] ratio) which is analogous to the [OI] G/R ratio (see Fig. 1). However, the [CI] line at 9824 Å was contaminated by telluric lines so that its surface brightness could not be accurately measured (Opitom et al. 2019). We thus used the known line ratio [CI] 9824/[CI] 9850 = 0.34 (Nussbaumer & Rusch 1979) to compute the [CI] line ratio which is reported in Table 2. Similarly, we have determined the observed intensity ratio of [NI] emission lines at 5198 and 5200 Å ([NI] ratio), which should be equal to the transition probabilities ratio of the excited states. Our full slit averaged [NI] ratio, which is 1.22 ± 0.09, is smaller by a factor of 2.2 than the theoretical branching ratio of 2.7 (Wiese & Fuhr 2007; see Section 5.6), whereas the full slit averaged [OI] red-doublet emission ratio of 3.03 ± 0.08 ([OI] ratio, i.e., 6300/6364) is consistent with the theoretically determined value (Wiese et al. 1996).

The measured and intrinsic widths of the different forbidden lines (full width at half maximum, FWHM) are presented in Table 3. The intrinsic FWHM is corrected for the instrumental broadening using the FWHM of the ThAr wavelength calibration lines using Equation 1 and the obtained intrinsic FWHMs are transformed into velocity (km s⁻¹) using Equation 2 that is

\[
FWHM_{\text{intrinsic}}(\lambda) = \sqrt{FWHM_{\text{observed}}(\lambda)^2 - FWHM_{\text{instrumental}}(\lambda)^2}
\]

(1)

\[
FWHM_{\text{intrinsic}}(\nu) = \frac{FWHM_{\text{intrinsic}}(\lambda)}{\lambda_{\nu} \sqrt{2\ln 2}}
\]

(2)

where \(\lambda_{\nu}\) corresponds to the wavelength of forbidden emission line. More details about determination of FWHMs are given in Decock et al. (2013). We assume the error on the FWHM_{\text{instrumental}}(\lambda) negligible. The FWHMs of different spectral emission lines that are measured on different nights were averaged and the dispersion of the measurements used to estimate the error. No significant dependence on the nucleocentric distance was found so that only measurements for the full slit are reported. The width of the green [OI] 5577 line is larger than the width of the [OI] red lines, which is similar to the observation made in water-dominated comets (Decock et al. 2015). A possible blend affecting [OI] 5577 Å was already investigated and discarded by Decock et al. (2015).
Table 1: Observed surface brightness of the various atomic forbidden emission lines in C/2016 R2 as a function of the nucleocentric projected distance.

| Distance (10^3 km) | [OI] 5577 | [OI] 6300 | [OI] 6364 | [CI] 8727 | [CI] 9850 | [NI] 5198 | [NI] 5200 |
|-------------------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| 0.3875±0.3875     | 9.82±0.49 | 26.62±1.06| 9.03±0.45 | 0.80±0.12 | 5.13±0.26 | 1.34±0.13 | 1.20±0.12 |
| 1.5500±0.7750     | 6.26±0.31 | 20.81±0.83 | 6.85±0.34 | 0.42±0.06 | 4.82±0.24 | 1.24±0.12 | 0.95±0.10 |
| 3.1000±0.7750     | 3.49±0.17 | 13.46±0.54 | 4.49±0.22 | 0.35±0.05 | 4.23±0.21 | 1.22±0.12 | 0.92±0.09 |
| 5.4250±1.5500     | 1.92±0.10 | 8.17±0.33 | 2.69±0.13 | 0.24±0.04 | 3.01±0.15 | 0.96±0.10 | 0.86±0.09 |
| 8.4475±1.4725     | 1.26±0.06 | 4.96±0.20 | 1.74±0.09 | 0.07±0.03 | 2.34±0.12 | 0.91±0.09 | 0.68±0.07 |
| Full Slit         | 3.31±0.07 | 11.00±0.22| 3.63±0.07 | 0.35±0.03 | 3.33±0.10 | 0.88±0.03 | 0.72±0.03 |

Notes. Surface brightness is in arbitrary units.

Table 2: Observed intensity ratios of atomic oxygen, carbon and nitrogen emissions in C/2016 R2 at different nucleocentric projected distances.

| Distance (10^3 km) | [OI] 5577 | [CI] 8727 | [NI] 5198 |
|-------------------|-----------|-----------|-----------|
| 0.3875±0.3875     | 0.28±0.03 | 0.12±0.02 | 1.12±0.22 |
| 1.5500±0.7750     | 0.23±0.02 | 0.07±0.01 | 1.31±0.26 |
| 3.1000±0.7750     | 0.19±0.02 | 0.06±0.01 | 1.33±0.27 |
| 5.4250±1.5500     | 0.18±0.02 | 0.06±0.01 | 1.12±0.22 |
| 8.4475±1.4725     | 0.19±0.02 | 0.02±0.01 | 1.34±0.27 |
| Full Slit         | 0.23±0.01 | 0.08±0.01 | 1.22±0.09 |

Notes. * (9824 + 9850) emission intensity is calculated by multiplying the observed 9850 Å emission intensity with a factor of 1.34. See the main text for more details.

3. Model calculations

The model calculations of the atomic oxygen green and red-doublet emissions intensities are explained in detail in our earlier work [Bhardwaj & Raghuram 2012; Raghuram & Bhardwaj 2013; 2014; Decock et al. 2015; Raghuram et al. 2016]. We have updated our model by including the atomic carbon and nitrogen emission lines. Here we present the model inputs considered for C/2016 R2 for the observational conditions of Opitom et al. (2019). We have done the model calculations when the comet was at distances of 2.8 au from the Sun and 2.44 au from the Earth. Since there is no information available on the radius of this comet, we assumed a typical value of 10 km for an Oort cloud comet.

3.1. Neutral distribution

The primary neutral composition of the cometary coma is taken as CO, CO₂, H₂O, N₂, and O₂. We have taken a CO gas production rate for this comet of 1.1 × 10^{29} s⁻¹ (Biver et al. 2018). The relative abundances of CO₂ and H₂O with respect to CO are taken as 18% and 0.3%, respectively, from McKay et al. (2019). Based on the measured ionic emission intensity ratios, the relative volume mixing ratio of N₂ is taken as 7% with respect to CO (Cochran & McKay 2018; Opitom et al. 2019; McKay et al. 2019). The recent Rosetta mass spectrometer in-situ measurements on 67P/Churyumov-Gerasimenko (Bieler et al. 2015; Altwegg et al. 2019) and subsequent investigation of data of the Giotto mass spectrometer from comet 1P/Halley (Rubin et al. 2015) have suggested that O₂ might be a common and an abundant primary species in comets. In order to incorporate the photo-
to dissociation of $\mathrm{O}_2$ in the model, we have assumed an abundance of 1% with respect to CO. However, we vary this value to study its impact on the calculations of the $[\mathrm{OI}]$ G/R ratio. We adopted an outflow speed of the neutral gas as $0.85 \times n_{\mathrm{e}}^{-0.5} = 0.5 \mathrm{~km/s}$ at heliocentric distance $r_h$ (Cochran & Schleicher 1993; de León et al. 2019), and spherical symmetry is considered in the calculations.

The model calculates the neutral density profiles of the primary cometary species using the following Haser’s formula, which assumes spherical expansion of volatiles into the space with a constant radial expansion velocity (Haser 1957).

$$n_i(r) = \frac{f_i Q_0}{4 \pi r^2 v_i \exp(-\beta_i r)}$$  \hspace{1cm} (3)

Here $n_i(r)$ is the number density of the $i$th neutral species at radial distance $r$ and $Q_0$ is the total gas production rate of the comet. $v_i$, $f_i$, and $\beta_i$ represent the expansion velocity, fractional composition, and inverse of scale height of the $i$th neutral species. We have considered $\mathrm{N}_2$ and CN as the primary species to produce $N(^2\mathrm{D})$ via dissociative excitation by both photons and photoelectrons. Assuming HCN is the parent source of CN, the neutral density profile of CN is calculated using Haser’s two-component formula (Haser 1957). For this calculation, we have taken HCN gas production as $4 \times 10^{24} \mathrm{s^{-1}}$ from the measurements of Biver et al. (2018). The role of other minor N-bearing species in producing $N(^2\mathrm{D})$ is found to be negligible as discussed later.

Aforementioned cometary gas parameters, which resemble the observational conditions of C/2016 R2, are taken as baseline inputs for the model calculations. These baseline parameters are summarized in Table 4. However, we vary the neutral abundances used in the model to discuss the effect on the calculated emission ratios.

### 3.2. Atomic and molecular parameters

A detailed explanation of the input cross sections and chemical network, which have been used to calculate $[\mathrm{OI}]$ forbidden emission lines, can be found in our earlier modelling work (Bhardwaj & Raghuram 2012). These model calculations account for various production and loss mechanisms of atomic oxygen in $^1\mathrm{S}$ and $^1\mathrm{D}$ states. We have added various production and loss reactions of metastable $C(^1\mathrm{D})$, $C(^1\mathrm{S})$ and $N(^2\mathrm{D})$ in the $[\mathrm{OI}]$ chemical network to calculate the atomic carbon and nitrogen emission line intensities. Table 5 shows these additional set of reactions, which are incorporated in our new chemical network.

### Table 3: Observed line widths of various atomic oxygen, carbon, and nitrogen forbidden emissions in C/2016 R2

| Line   | Full width at half maximum (FWHM) | Observed ($\lambda$) | Intrinsic ($\lambda$) | Intrinsic ($\mathrm{km\ s^{-1}}$) |
|--------|----------------------------------|---------------------|---------------------|----------------------------------|
| [OI] 5577 | 0.0982±0.0017 | 0.0773±0.0017 | 2.50±0.05 |
| [OI] 6300 | 0.1019±0.0010 | 0.0702±0.0010 | 2.01±0.03 |
| [OI] 6564 | 0.1025±0.0010 | 0.0710±0.0010 | 2.01±0.03 |
| [CI] 8727 | 0.1569±0.0048 | 0.1290±0.0048 | 2.56±0.10 |
| [CI] 8780 | 0.1611±0.0023 | 0.1069±0.0023 | 1.95±0.04 |
| [NI] 5198 | 0.0677±0.0158 | 0.0321±0.0158 | 1.11±0.55 |
| [NI] 5200 | 0.1011±0.0206 | 0.0817±0.0206 | 2.83±0.72 |

We have taken the electron impact cross section of $N_2$ producing $N(^2\mathrm{D})$ from Tabata et al. (2006). To incorporate production of $N(^2\mathrm{D})$ via photodissociation of $N_2$, following the approach of Fox (1993), we have assumed an average photodissociation yield of 0.32. The impact of this assumption on the calculation of $[\mathrm{CI}]/[\mathrm{NI}]$ emission ratio will be discussed in the later section. We have taken the photodissociation cross sections of CN producing $C(^1\mathrm{D})$ and $N(^2\mathrm{D})$ from El-Qadi & Stancil (2013). The photodissociation cross section of CO producing $C(^1\mathrm{S})$ has never been reported in the literature. In order to incorporate this production path in the model, we assumed that 0.5% of the total CO absorption cross section, above the dissociation threshold energy, leads to $C(^1\mathrm{S})$ formation. However, we vary this value to fit the observed carbon emission intensity ratios, as discussed later. The collisional quenching rate coefficients of $N(^2\mathrm{D})$ by $\mathrm{H}_2\mathrm{O}$, $\mathrm{CO}$, $\mathrm{CO}_2$, and $\mathrm{O}_2$ are taken from Herron (1999), whereas, for $C(^1\mathrm{D})$ they are taken from Schofield (1979).

#### 3.3. Determination of emission intensity ratios

The solar radiation flux ($\phi_{\mu l} (\lambda)$) in the wavelength region 5–1900 Å is degraded in the cometary coma using the Beer-Lambert’s law. The photoelectron production rate spectrum is calculated as a function of electron energy at different radial distances. By incorporating the Analytical Yield Spectrum (AYS) approach, which accounts for the degradation of electrons in the cometary coma based on the Monte Carlo technique, the suprathermal flux ($\phi_e (r, E)$) is calculated as a function of electron energy ($E$) at the radial distance $r$. More details about the calculation of suprathermal electron flux are given in Bhardwaj & Raghuram (2012).

By using the model degraded photon flux and steady state suprathermal electron flux profiles with the corresponding photon and electron impact excitation cross sections, we determined the volume production rate profiles for the different metastable state species in the coma using the following equations.

$$P_{ij,\text{photon}}(r) = n_i(r) \int_{E_{\text{min}}}^{E_{\text{max}}} \sigma_{ij,\text{photon}}(\lambda) \phi_{\mu l}(\lambda) e^{-\tau(\lambda, r)} d\lambda$$  \hspace{1cm} (4)

$$P_{ij,\text{electron}}(r) = n_i(r) \int_{E_{\text{min}}}^{E_{\text{max}}} \sigma_{ij,\text{electron}}(E) \phi_e(r, E) dE$$  \hspace{1cm} (5)

Where $P_{ij,\text{photon}}(r)$ and $P_{ij,\text{electron}}(r)$ are the volume production rates of the $i$th metastable species due to the photon and electron impact dissociative excitation of the $i$th cometary neutral species, respectively. $\sigma_{ij,\text{photon}}$ and $\sigma_{ij,\text{electron}}$ are the respective photon and electron impact dissociative excitation cross sections of the $i$th neutral species producing the $j$th metastable state. $\lambda_{\text{min}} = 5\lambda$ ($E_{\text{min}} = 0$ eV) and $\lambda_{\text{max}} = 1900$ Å ($E_{\text{max}} = 100$ eV) are the respective lower and upper integration limits of the wavelength (energy). $\tau(\lambda, r)$ is the optical depth of the medium for the photons of wavelength $\lambda$ at the radial distance $r$. Table 6 shows the calculated photodissociation frequencies of the major cometary volatiles producing different metastable species at 1 au. The loss rate profiles of these excited states, which are mainly due to collisional quenching and radiative decay, are determined by incorporating the collisional chemistry in the coma. The major photochemical pathways, producing the forbidden emission lines, are schematically presented in Fig. 3.

The calculated production and loss rate profiles have been used to obtain the number densities of metastable species ($n_j$) by...
solving the following continuity equation.

\[ \frac{1}{r^2} \frac{d}{dr} \left( r^2 n_j v_j \right) = P_j - L_j \] (6)

Here \( r \) is the radial distance from the cometary nucleus, \( v_j \) is the radial transport velocity, and \( P_j \) and \( L_j \) are the respective total production and loss rates of the \( j \)th metastable species. The transport velocities of the metastable species are taken from the measured intrinsic line widths (see Table 3). The calculated density profiles are converted into volume emission rates by multiplying the corresponding Einstein transition probabilities of the different emissions. The volume emission rate profiles are integrated along the line of sight to obtain surface brightness profiles. We have also accounted for the optical seeing effect in determining the emission ratio as described in Decock et al. (2015). As explained in the earlier section, seeing during the observations was 0.9' for [OI], [NI] emissions and 1.0' for [CI] emissions.

We have determined the [OI] G/R ratio and emission intensity ratios of C(1)D to N(2)D (hereafter [CI]/[NI] ratio), and carbon lines (hereafter [CI] ratio) using the following equations.

Table 4: Summary of the baseline input parameters used in the model

| Parameter | Value |
|-----------|-------|
| CO gas production rate \( Q_{CO} \) | \( 1.1 \times 10^{29} \) s\(^{-1} \) |
| Neutral abundances\(^{\dagger} \) | CO\(_2\) (18\%), H\(_2\)O (0.3\%), O\(_2\) (1\%), and N\(_2\) (7\%) |
| Heliocentric distance of the comet | 2.8 au |
| Geocentric distance of the comet | 2.44 au |
| Neutral gas expansion velocity | 0.5 km/s |

Notes. \(^{\dagger}\)The neutral relative abundances in the parentheses are with respect to the CO production rate.

Table 5: Production and loss reactions of N(2)D, C(1)D and C(1)S incorporated in the chemical network of coupled-chemistry emission model.

| Reaction | Rate Coefficient\(^{\dagger} \) \((\text{cm}^3 \text{ molecule}^{-1} \text{s}^{-1} \text{ or s}^{-1})\) | Reference |
|----------|------------------------------------------------|-----------|
| \( h^+ + N_2 \rightarrow N(2)D + N \) | \( 3.0 \times 10^{-7} \) | This work |
| \( h^+ + CN \rightarrow N(2)D + C \) | \( 1.0 \times 10^{-6} \) | This work |
| \( h^+ + CO \rightarrow C(1)D + O \) | \( 7.6 \times 10^{-8} \) | This work |
| \( h^+ + CN \rightarrow C(1)D + N \) | \( 2.0 \times 10^{-6} \) | This work |
| \( h^+ + CO \rightarrow C(1)S + O \) | \( 1.5 \times 10^{-10} \) | This work |
| \( e_{ph} + N_2 \rightarrow N(2)D + N \) | Calculated | This work |
| \( e_{ph} + CN \rightarrow N(2)D + C \) | Calculated | This work |
| \( e_{ph} + CO \rightarrow C(1)D + O \) | Calculated | This work |
| \( e_{ph} + CN \rightarrow C(1)D + N \) | Calculated | This work |
| \( e_{ph} + CO \rightarrow C(1)S + O \) | Calculated | This work |
| \( N(2)D + H_2O \rightarrow N + H_3O \) | \( 4.0 \times 10^{-11} \) | Herron (1999) |
| \( C(1)D + H_2O \rightarrow C + H_3O \) | \( 3.6 \times 10^{-13} \) | Herron (1999) |
| \( C(1)D + CO \rightarrow C + H_2O \) | \( 1.9 \times 10^{-12} \) | Herron (1999) |
| \( N(2)D + O_2 \rightarrow N + O_2 \) | \( 5.2 \times 10^{-12} \) | Herron (1999) |
| \( N(2)D + N_2 \rightarrow N + N_2 \) | \( 1.7 \times 10^{-14} \) | Herron (1999) |
| \( N(2)D \rightarrow N + h\nu_{5200 \text{ & } 5198 \text{ Å}} \) | \( 2.78 \times 10^{-5} \) | Wiese & Fuhr (2009) |
| \( C(1)D + H_2O \rightarrow C + H_2O \) | \( 1.7 \times 10^{-11} \) | Schofield (1979) |
| \( C(1)D + CO \rightarrow C + H_2O \) | \( 3.7 \times 10^{-11} \) | Schofield (1979) |
| \( C(1)D + CO \rightarrow C + H_2O \) | \( 1.6 \times 10^{-11} \) | Schofield (1979) |
| \( C(1)D + O_2 \rightarrow C + O_2 \) | \( 2.6 \times 10^{-11} \) | Schofield (1979) |
| \( C(1)D + N_2 \rightarrow C + N_2 \) | \( 4.2 \times 10^{-12} \) | Schofield (1979) |
| \( C(1)D \rightarrow C + h\nu_{9824 \text{ & } 9850 \text{ Å}} \) | \( 2.91 \times 10^{-4} \) | Wiese & Fuhr (2009) |
| \( C(1)S + H_2O \rightarrow C + H_2O \) | \( 1 \times 10^{-16} \) | Schofield (1979) |
| \( C(1)S + CO \rightarrow C + H_2O \) | \( 1 \times 10^{-16} \) | Schofield (1979) |
| \( C(1)S + CO \rightarrow C + H_2O \) | \( 6 \times 10^{-14} \) | Schofield (1979) |
| \( C(1)S + N_2 \rightarrow C + H_2O \) | \( 3 \times 10^{-15} \) | Schofield (1979) |
| \( C(1)S \rightarrow C + h\nu_{6727 \text{ Å}} \) | 0.6 | Wiese & Fuhr (2009) |

Notes. \(^{\dagger}\)Photodissociation frequencies presented in this table are calculated at 1 au; \( e_{ph} \) is photoelectron and \( h\nu \) is solar photon.
4. Results

The calculated production rate profiles of atomic oxygen in $^1S$ (top panel) and $^1D$ (bottom panel) states are presented in Fig. 4.

This calculation shows that the formation of both $^1S$ and $^1D$ in the coma of C/2016 R2 occurs mainly due to the photodissociation of CO$_2$. The photodissociation of CO contributes to about 20% of the total $^1S$ production rate. The contribution of the photodissociative excitation of other oxygen-bearing species to the total $^1D$ production rate is small ($<10\%$), within the observed projected distance, i.e. $10^4$ km. The electron impact dissociative excitation of oxygen-bearing species plays a minor role in producing these atomic oxygen metastable states.

The calculated loss frequency profiles of atomic oxygen in $^1S$ (top panel) and $^1D$ (bottom panel) states are presented in Fig. 5. Radiative decay is the primary loss source of $^1S$ in the entire coma, as compared to the collisional quenching. Whereas, the CO$_2$ collisional quenching is the significant loss process for $^1D$ for radial distances below 500 km. Above this radial distance, radiative decay is the prominent loss source.

The modelled $^1D$ and N$^2D$ production rate profiles for different formation pathways are presented in Fig. 6. This calculation shows that the photodissociation of CO and N$_2$ are the major formation processes of C$^1D$ and N$^2D$, respectively, whereas the contribution of the electron impact dissociative excitation to the total production rate is negligible. The role of the CO$_2$ photodissociation is minor (more than three orders of magnitude smaller than the CO photodissociation) in the total formation of C$^1D$. Similarly, these calculations also show that the contribution from the dissociative excitation of CN, in producing C$^1D$ and N$^2D$, is negligible to the total formation rate.

Modelling loss frequency profiles of these excited states are presented in Fig. 7 and show that significant collisional quenching of C$^1D$ and N$^2D$ occurs via CO (>90% of the total), for the radial distances below $3 \times 10^4$ km. Above this radial distance, radiative decay is the major loss mechanism for both C$^1D$ and N$^2D$.

The modelled $^1S$ production rate profile, via photodissociation of CO, and the loss profiles due to collisional quenching and radiative decay are presented in Fig. 8. Radiative decay of $^1S$ is found to be the dominant loss channel, which leads to [CI] 8727 Å emission, with an efficiency several orders of magnitude higher compared to the collisional quenching.

We have calculated the timescale profiles for the loss of excited states due to both collisional quenching and radiative decay (chemical loss), which is reciprocal to the total loss frequency profiles as determined in Figs. 5, 7, and 8. The timescale for transport (advection) for the excited species is determined as $t_{adv}(r) = r \times \langle v_j(r) \rangle^{-1}$, where $v_j$ is the mean radial velocity of the $j$th excited species as determined from the observations (see Table 6). These modelled timescale profiles for chemical loss and transport are plotted in Fig. 9. It can be noticed in this figure that the $^1S$ and C$^1D$ chemical lifetimes are smaller than the time required for transport by more than an order of magnitude for radial distances larger than 100 km. The timescales of C$^1D$ due to chemical loss and transport are equal at the radial distance of 300 km, whereas this equality occurs at a radial distances of 100 and $2 \times 10^4$ km for C$^1D$. The N$^2D$ timescale for transport is smaller than the chemical lifetime in the entire coma.

After incorporating the previously mentioned production and loss mechanisms, we have solved the one-dimensional continuity equation (Eq. 5), to calculate the radial density profiles of O$^1S$, O$^1D$, C$^1D$, N$^2D$, and C$^1S$. They are plotted in Fig. 10. The peaks of O$^1S$ and C$^1S$ number densities occur close to the surface of the nucleus at radial distances below 20 km. The calculated N$^2D$, C$^1D$ and O$^1D$ density profiles have broad peaks at around 100 km radial distance, due to their long radiative lifetimes.

In the bottom panel of Fig. 11, we compare the modelled [OI] green to red-doublet ratio with the observations. Using the baseline parameters as discussed in Section 3, we find that our modelled values are higher by a factor 3 when compared to observation (hereafter Case-A). If we consider an O$_2$ abundance of 30% with respect to the CO production rate (hereafter Case-B), instead of our assumed 1% in the baseline, our calculated [OI] G/R ratio is consistent with the observed emission ratio for radial distances below 1000 km. Above this radial distance the modelled ratio is about 40% higher than the observations. In this case, photodissociation of CO$_2$ and O$_2$ are the major sources of O$^1S$ and O$^1D$, respectively. Due to the uncertainty in the CO$_2$
photodissociative excitation cross section producing \( \text{O}^1\text{D} \), as discussed in the next section, we have increased the photodissociation rate by a factor of about 3 in our model calculations (hereafter Case-C). For this case, the modelled [OI] green to reddoublet emission ratio is in agreement with the observations.

Similarly, by using the baseline parameters as discussed in Section 5 the modelled [CI]/[NI] emission ratio profiles are found to be higher by a factor 3 than the observations (hereafter Case-D, and see top panel of Fig. 11). Due to the uncertainty in the photodissociative excitation cross section, we have decreased the photodissociation rate of CO producing \( \text{C}^1\text{D} \) by a factor of 4 (hereafter Case-E) in the model calculations. With these new dissociation rates, we find that the calculated emission ratios are in agreement with the observations. When we increase the \( \text{N}_2 \) dissociative excitation rate producing \( \text{N}^2\text{D} \) by a factor of about 3 (hereafter Case-F), we find that the modelled [CI]/[NI] emission ratio is consistent with the upper limit of the observations. The conditions for different case studies are summarized in Table 7.

If we assume that CO is the only parent source of the atomic carbon emissions, then the observed [CI] ratio should be equal to the ratio of the average branching fractions of CO producing \( \text{C}^1\text{S} \) and \( \text{C}^1\text{D} \). As described in the earlier section, we have modelled the \( \text{C}^1\text{S} \) density and calculated the 8727 Å emission intensity by assuming that 0.5% of the total CO absorption cross section leads to \( \text{C}^1\text{S} \) formation. Our modelled [CI] emission ratios for different yields along with the observation are plotted in Fig. 12 as a function of the nucleocentric projected distance. We find that the calculated [CI] ratio profiles are consistent with the observations when we vary the CO photodissociation yield between 1 and 1.5%.

5. Discussion

The photochemical processes such as dissociative excitation of cometary coma species, collisional chemistry and radial transport of metastable species determine the observed emission intensity ratios. When we use our baseline input parameters, as explained in Section 5 the calculated [OI] G/R and [CI]/[NI] ratios are higher by a factor of about 3 compared to the observations. In order to study the discrepancies between the modelled and the observed emission ratios, we examined the effects of uncertainties associated with the input parameters, which are discussed below.

5.1. Effect of the neutral species abundances

In a water-dominated coma, \( \text{H}_2\text{O} \) photodissociation is the major source of \( \text{O}^1\text{D} \). But the observations of Biver et al. (2018) showed that \( \text{H}_2\text{O} \) abundance with respect to CO can not be more than 10%. The recent McKay et al. (2019) observations suggest much lower water abundance (0.3% with respect to CO), which is also observed by Opitom et al. (2019). Even by assuming an \( \text{H}_2\text{O} \) abundance of 10% relative to CO, we find that \( \text{H}_2\text{O} \) is playing no role in determining the [OI] G/R ratio. This calculation suggests that CO2 mainly governs both the green and reddoublet atomic oxygen emission intensities and the contribution from other excitation processes is negligible. The derivation of water production rates based on the observed oxygen emission lines would of course lead to an over estimation of \( \text{H}_2\text{O} \) abundance in this comet.

![Fig. 4: Calculated O(1S) (top panel) and O(1D) (bottom panel) production rate profiles, for different photon and electron impact dissociative excitation reactions of major cometary volatiles, in C/2016 R2 when it was at 2.8 au from the Sun. The total gas production rate of CO is taken as 1.1 x 10^29 s^-1 with 0.3% \( \text{H}_2\text{O} \), 18% \( \text{CO}_2 \) and 1% \( \text{O}_2 \) with respect to carbon monoxide. hv represents a solar photon and e ph is a suprathermal electron.](image-url)
Biver et al. (2018) observed several other O-bearing species such as CH\textsubscript{3}OH, H\textsubscript{2}CO, HNCO, NH\textsubscript{2}CHO, CH\textsubscript{3}CHO, HCOOH, SO, and SO\textsubscript{2} in this comet. The branching ratios as determined by Huebner et al. (1992) suggest that these species do not have direct production channels for O(1S) and O(1D). Moreover, these species are observed with very low abundance, more than two orders of magnitude smaller than CO (Biver et al. 2018). Hence, the contribution of these species producing [OI] emission lines can be neglected.

The modelling work of Cessateur et al. (2016a) has suggested that O\textsubscript{2} can play a significant role in determining the [OI] G/R ratio. By incorporating a small O\textsubscript{2} abundance, of 1% of the CO production rate, we find that the contribution of O\textsubscript{2} dissociative excitation is very small (more than two orders of magnitude to the total) in producing O(1S) whereas it is the third most important source of O(1D) for radial distances above 30 km (see Fig. 4). By increasing the O\textsubscript{2} abundance to 4% of CO, we find that about 30% of O(1D) is produced from the photodissociation of O\textsubscript{2} and 50% of the total is coming from CO\textsubscript{2}. In this case, O(1S) is mainly (> 80%) produced from the photodissociation of CO\textsubscript{2} and the role of O\textsubscript{2} is small (< 1%). This calculation suggests that O\textsubscript{2} is a potential source of O(1D), after CO\textsubscript{2}, when its abundance is substantial (>5%).

The in-situ measurements of the Rosetta mass spectrometer have shown that O\textsubscript{2} is present in the coma of comet 67P with a mean abundance of about 2% (Altwegg et al. 2019). During the Rosetta mission, Bieler et al. (2015) have also shown that the O\textsubscript{2} relative abundance with respect to H\textsubscript{2}O can be as high as 15%. It should be noted that the mass spectrometer abundances are based on the observations made at the spacecraft position. However, the Alice UV spectrometer on-board Rosetta can observe spatial distribution of neutrals in the entire cometary coma based on the emission intensities (Feldman et al. 2018). From Alice limb view observations, Keeney et al. (2017) found that the O\textsubscript{2}/H\textsubscript{2}O relative abundance ratio in 67P coma varies between 11–68%, with a mean value of 25%. These observations suggest that O\textsubscript{2} could be present in large amount in cometary comae. We then have increased the O\textsubscript{2} relative abundance to 30% of CO to verify its impact on the [OI] G/R abundance ratio. By considering such a large O\textsubscript{2} abundances, we have shown that the model calculated [OI] G/R ratio is close to the observation (see bottom panel of Fig. 11) for radial distances below 10\textsuperscript{3} km. However, the calculated emission ratios are higher by about 40% compared to the observation in the non-collisional zone, i.e., for radial distances larger than 10\textsuperscript{3} km (also see Fig. 5). This calculation sug-

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**Fig. 5:** Modelled O(1S) (top panel) and O(1D) (bottom panel) loss frequency profiles via collisional quenching of the major cometary volatiles and radiative decay in C/2016 R2. The input conditions are the same as in Fig. 4.

**Fig. 6:** Calculated C(1D) (top panel) and N(1D) (bottom panel) production rate profiles, for different photon and electron impact dissociative excitation reactions of the major cometary volatiles, in C/2016 R2. Photodissociation and electron impact dissociation of CN producing N(1D) production rate profiles are plotted after multiplying them by a factor 10. The input conditions are the same as explained in Fig. 4. $\nu$ represents a solar photon and $e_{ph}$ is a suprathermal electron.
suggests that there is a possibility of having a significant amount of molecular oxygen (about 30% relative to CO) in this comet.

Similarly, we have studied the discrepancy between the modelled and observed [CI]/[NI] emission ratio by varying the neutral abundances. We have considered CO2 and CO as the primary molecules to produce C(1D) and CN and N2 for N(2D). The role of CO2 in producing C(1D) is negligible compared to that of CO. This is mainly due to the significant difference between the photodissociative excitation cross sections of CO and CO2 producing atomic carbon (about two orders of magnitude, see [Huebner et al. 1992]). C(1D) can be produced directly from the dissociation of CO whereas it is a two-step process for CO2. By increasing the CO2 abundance equal to that of CO, we find that CO is still the dominant source of C(1D), which suggests that [CI] emission lines are governed only by the CO photodissociation and the role of CO2 in producing carbon emission lines can be neglected.

In order to match the observed [CI]/[NI] emission ratio, the N2/CO volume mixing ratio should be altered by a factor of 3 either by decreasing the CO or by increasing the N2 production rates. Since the comet is moving towards the Sun, we do not expect a decrease in the CO sublimation rate during the observation period. However, large N2 abundances (>10%) are not expected either, unless there is a cometary outburst during the period of observation. Moreover, different observations have confirmed that the N2 abundance in this comet is about 7% relative to CO (Cochran & McKay 2018; Biver et al. 2018; Opitom et al. 2019).

Hence, we do not expect this comet to have a large enough N2 abundance (>10%) to produce the observed [CI]/[NI] emission ratio. We have also investigated other N-bearing species which can produce N(2D) with a significant amount. Singh et al. (1991) proposed that the formation of metastable nitrogen atoms in 2-D state is possible due to the photodissociation of CN. But our modelled production rate profiles of N(2D) show that the contribution from CN is negligible compared to the photodissociation of N2 (see Fig. 6). Moreover, [Opitom et al. 2019] estimated the CN production rate as 3 x 10^11 s^-1, which is five orders of magnitude smaller than the CO gas production rate and cannot be the dominant source of [CI] and [NI] emission lines. Similarly, the observations of various N-bearing species viz., HCN, CH3CN, H3CN, HNCO, NH3CHO by [Biver et al. 2018] and [McKay et al. 2019] show that their relative abundances in the coma are very small (<1%) compared to N2, while the [Huebner et al. 1992]
compilation of photodissociation cross sections does not suggest direct dissociative excitation channels to produce N(2D). Hence, we conclude that the atomic nitrogen emission is only governed by the photodissociation of N2 in C/2016 R2.

The Opitom et al. (2019) observations clearly show that C2 and C3 molecules are only present in negligible amount in this comet. Unlike the major volatiles, C2 and C3 are not directly produced in the coma via sublimation of ices in the nucleus. The formation and destruction of these species is involved with a complex chemistry. By considering the long-chain carbon-bearing species in the coma, Hölscher (2015) has studied the density distribution of C2 and C3 in the comae of different comets. Based on these calculations, we estimated that the production rate of C(1D) via dissociation of C2 and C3 is smaller than the photodissociation rate of CO by more than three orders of magnitudes. However, the calculation of C2 and C3 number density profiles using the complex chemical network as described by Hölscher (2015) is beyond the scope of the present work.

5.2. Effect of the cross sections

The uncertainty in the photodissociation cross section of CO2 producing O(1D) could be the reason of the difference between the modelled and the observed [OI] G/R ratio. Lawrence (1972) experimentally determined the photodissociation yield of CO2 producing O(1D) as small as 1 in the wavelength range 1000–1150 Å. We have considered this measured yield to calculate the CO2 dissociation rate to produce O(1D). The cross section for O(1D) formation via CO2 dissociative excitation is not reported in the literature, as noticed by Huestis & Slanger (2006). Huebner et al. (1992) constructed these photodissociation cross sections of CO2 assuming a dissociation branching ratio close to 1 in the wavelength region 1000–1665 Å. This assumption contradicts the Lawrence (1972) experimentally determined branching ratio. Both O(1D) and O(1S) can not be produced with 100% yield in the same wavelength region. Slanger et al. (1977) also measured the quantum yield of O(1S) for photodissociation of CO2 and found a sudden dip in the yield around 1089 Å. Hence, there is an uncertainty associated with the Huebner et al. (1992) recommended cross sections which can impact our calculated
[O I] G/R emission ratio. There are several recent experimental developments in detecting O(1D) via the photodissociation of CO₂ (Sutrada et al. 2017; Li et al. 2015; Song et al. 2014; Schmidt et al. 2013; Gao & Ng 2019; Pan et al. 2011). But these measurements are limited to a small energy range (<1 eV) and do not provide the O(1D) yield over a wide wavelength range (from dissociation threshold to 1000 Å) which is essential to determine the average dissociation ratio of O(3S)/O(1D) in the photodissociation of CO₂.

As discussed in the earlier section, the photodissociation of CO₂ is the major source of O(3S) in the coma. This is mainly due to the larger photodissociation rate of CO₂ than CO and H₂O (a factor around 20 higher compared to other O-bearing species, see Table 2, Fig. 4 and Huebner et al. 1992). Similarly, CO₂ can also produce O(1D) by a factor of 3 more efficiently than any other O-bearing species. Hence, if CO₂ is the major production source of oxygen lines, then the observed [O I] G/R ratio in the non-collisional region (i.e. above 10⁴ km, see Fig. 5) should match the ratio of CO₂ dissociation rates producing O(3S) and O(1D).

Our calculations suggest that the photodissociation of CO₂ is the second most important source of [OI] emission lines (see Fig. 4). Since most of the O(3S) and O(1D) are produced from CO₂, the uncertainties associated with the CO₂ dissociation cross sections can not play a significant role in determining the [OI] G/R ratio. Moreover, the respective dissociation threshold energies of CO, producing O(1D) and O(3S) states are 14.35 and 16.58 eV, which are more than the ionization threshold i.e., 14 eV. Due to the proximity of the threshold energies, most of the UV radiation absorbed by CO turn into ion rather than producing O(3S) and O(1D). Hence CO is not an efficient source of [OI] emission lines, when compared to CO₂, to determine the [OI] G/R ratio.

In our earlier work, we have theoretically determined [OI] G/R ratios of 0.04, 0.6, 1, and 0.04 for the photodissociation of H₂O, CO₂, and CO₂, respectively (Bhardwaj & Raghuram 2012; Raghuram & Bhardwaj 2013; Raghuram et al. 2016). If CO₂ is the only source of these emission lines, by using the photodissociation cross sections from the baseline model (also see Bhardwaj & Raghuram 2012), our model suggests that the [OI] G/R ratio should be around 0.6 for the non-collisional region. But the observed ratio in this comet is only about 0.2 between radial distances of 2 × 10⁴ and 1 × 10⁵ km, where the radiative decay is the only loss process (see Fig. 11). We will show in the next section that the collisional quenching can alter the observed [OI] G/R ratio only for radial distances less than 2 × 10⁵ km (see Fig. 5). Since CO₂ is the major source of [OI] emissions and there is a large uncertainty associated with the CO₂ photodissociation cross section in producing O(1D), we have increased the photodissociation rate by a factor of 3 (see Case-C in Fig. 11). For this value of the photodissociation rate, the observed and modelled [OI] G/R ratios are consistent. Hence, based on the comparison between the modelled and observed [OI] G/R ratio profiles, we suggest to increase the Huebner et al. (1992) recommended photodissociation cross section of CO₂ producing O(1D) by a factor of 3.

In our modelling calculations on different comets at different heliocentric distances, we have shown that H₂O is the major source of O(1D) (Bhardwaj & Raghuram 2012; Raghuram & Bhardwaj 2013, 2014; Decock et al. 2015; Raghuram et al. 2016). Even though the photodissociation rate of H₂O producing O(1D) is comparable (a factor of 1.5 higher) to that of CO₂ (see, Huebner et al. 1992), CO₂ became the prominent source of green and red-doublet emission lines due to the very low water abundance in this comet. Hence, this new value of CO₂ dissociation rate producing O(1D) does not contradict the conclusions of our earlier calculations done in the water-dominated cometary coma.

Similarly, the discrepancy between the modelled and the observed [CI]/[NI] emission ratios could also be due to the uncertainties in the photodissociation cross sections of CO and N₂. Shi et al. (2018) recently determined the branching ratio for CO producing C(1D) in the wavelength range 905–925 Å. They found that the pre-dissociation of CO leads to about 20% formation of C(1D) and the rest into carbon and oxygen ground and 1D states, respectively. Huebner et al. (1992) do not account for the pre-dissociation channels in the formation of C(1D). The cross section is constructed based on the assumptions of McElroy & McConnell (1971). By decreasing the CO photodissociation rate by a factor of 4, we find that the modelled [CI]/[NI] emission ratio is consistent with the observation (see Case-E in Fig. 11). This calculation shows that the uncertainty associated with the Huebner et al. (1992) CO photodissociation cross section could be a reason for the discrepancy between the modelled and the observed ratios. So we suggest that the photodissociation cross section of CO producing C(1D) should be revised based on the recently determined branching ratios.

We have taken a mean average branching ratio of N(2D) of 0.32 following the approach of Fox (1993) calculations on Mars and Venus atmospheres. Song et al. (2016) measured branching ratios for the photodissociation of N₂ producing N(2D) in the wavelength region 816.3–963.9 Å as high as 1. By increasing the N₂ photodissociation rate by a factor of 3, we find that the modelled [CI]/[NI] emission ratio is consistent with the upper limit of the observations (see Case-F in Fig. 11). These calculations suggest that the uncertainties associated with the photodissociation cross sections of CO and N₂ are the main reason for the discrepancy between the modelled and the observed [CI]/[NI] emission ratios.

Besides the cross sections of neutral species, the modelled photodissociation frequencies also depend on the solar activity. Considering the solar activity, Huebner et al. (1992) have shown that the calculated photodissociation frequencies of neutrals can vary by a factor of about 2 from solar minimum to maximum. Since the observations of C/2016 R2 are all done in February 2018, which is during a minimum range of time and solar minimum condition, we do not expect the solar activity to significantly influence the modelled dissociation frequencies and subsequently the calculated emission ratios.

5.3. Effect of collisional quenching rates

The collisional quenching of atomic oxygen can alter the observed emission ratio for radial distances smaller than 2 × 10⁵ km (see Fig. 5). Owing to a short radiative lifetime (0.75 s; Wiese & Fuhr 2009), the collisional quenching of O(3S) is not significant in the entire coma. But for O(1D), the quenching is an important loss process up to radial distances of 2 × 10⁶ km (see Fig. 5). By assuming a collisional quenching source of O(1D), which is an order of magnitude higher than that of CO₂, we could alter the G/R ratio only up to radial distances = 10⁵ km by a factor of 2. Hence, the observed [OI] G/R ratio, beyond 10⁵ km radial distances, is purely a function of dissociative excitation of CO₂.

The collisional quenching is significant for both C(1D) and N(2D) due to their radiative lifetimes of about 3500 s and 10 hrs, respectively, up to radial distances of 2 × 10⁶ km (see Fig. 7). But we could not find a significant change in the calculated [CI]/[NI]
emission ratios by varying the quenching rates. Our calculated lifetime profiles of these excited species show that the transport of N(2D) is a more important loss process than the collisional quenching in the coma (see Fig. 9). In this figure, it can be noticed that the C(1D) collisional quenching can affect the modelled [CI]/[NI] emission ratio only for radial distances below 50 km. By assuming an unknown collisional reaction in the coma with a quenching rate of an order magnitude higher than that of CO, we find the modelled [CI]/[NI] emission ratio is not changing for radial distances beyond 4 × 10^3 km.

The collisional quenching is a strong barrier inhibition in measuring the photodissociation crosssection of species producing metastable states. Due to the long lifetimes and also the excess velocities acquired during dissociation, most of the metastable species drift away from the spectrometer field of view and also collide with the walls of the chamber which makes very difficult to measure such cross sections in the laboratory (Kami et al. 2003). Owing to natural vacuum conditions, the metastable species produced via cometary species can survive longer times and will be transported to large radial distances from the origin of production before they de-excite to ground state via radiative decay. Hence in the absence of collisions, the observed cometary forbidden emissions lines can be used to study the dissociation properties of the respective parent species which makes comets unique natural laboratories.

5.4. Effect of transport

When the mean lifetime of a species is more controlled by collisions or radiative decay than radial transport, we can consider that the species is under photochemical equilibrium (PCE). The calculated lifetime profiles presented in Fig. 9 show that O(1S) and C(1S) are in PCE in the entire cometary coma. The transport of C(1D) and O(1D) is important for radial distances above 50 and 100 km, respectively. Due to the large radiative lifetime of N(2D) (about 10 hrs), the transport plays a significant role in determining its number density in the coma. These calculations suggest that the role of transport in determining the [OI] G/R ratio is insignificant whereas it is important for the [CI]/[NI] emission ratio.

Huebner et al. (1992) have determined the mean excess energies released in the photodissociation of N₂ and CO as 3.38 and 2.29 eV, respectively. Using these calculated excess energies, we estimated the mean ejection velocities of N(2D) and C(1D) as 4.77 and 4.59 km/s, respectively, (cf. Wu & Chen 1993). By using these theoretically estimated mean velocities in the model, we found our modelled [CI]/[NI] emission ratio is higher by a factor of 2. If we assume that our estimated mean excess velocities of C(1D) and N(2D) are realistic, then a factor of 2 in CO photodissociation rate will be sufficient to explain the observed [CI]/[NI] ratio. But our observed line widths suggest that C(1D) and N(2D) did not acquire velocities as calculated by Huebner et al. (1992).

Our theoretically estimated N(2D) and C(1D) excess velocities are based on the calculation of Huebner et al. (1992). These values are higher than our mean velocities derived from the observations by about a factor of 2 (see Table 3). However, it should be noticed that Huebner et al. (1992) have used a reference solar flux for solar minimum condition to determine the excess energy released in the photodissociation. The solar flux as observed by the comet determines the mean excess energy released in the photodissociation and subsequently the widths of the spectral lines. The determination of excess energies released in the photochemical process requires the knowledge of the solar radiation flux interacting with the coma and also the absolute branching fractions over a wide wavelength range, which are the strong constraints to compute the mean excess velocities.

The role of transport on O(1D) and O(1S) is not significant in determining the [OI] G/R ratio. This can be understood from the calculations of the timescales for chemical lifetime and transport presented in Fig 2. We have calculated density profiles of all the metastable species using the derived excess velocities from the observed line widths. The Huebner et al. (1992) theoretical calculations at 1 au suggest that excess energies of about 4 eV will be released in the photodissociation of CO₂ producing O(1D). Around 65% of excess energy released in the dissociation would produce atomic oxygen with an excess velocity of about 5 km/s. By increasing the radial velocity of the metastable species to about 5 km/s, our calculated [OI] G/R ratio is higher by a factor of 5 compared to the observations. The role of transport in determining the O(1S) density is negligible due to its small lifetime of about 1 s, whereas it can affect O(1D) up to radial distances of 10^4 km. Due to the lack of measured cross sections of O(1D) via CO₂ it is difficult to determine the excess energy released in the photodissociation.

5.5. Line widths

The observed FWHMs of the emission lines mainly depend on the mean kinetic energy of the excited species which are produced in the dissociative excitation. Our calculations suggest that the influence of collisional quenching on the line width is up to radial distances of 10^4 km (see Figs. 3 and 6). In the observed spectra, we find that the measured line widths of the observed emissions are not varying significantly as a function of the nucleocentric distance. Moreover, the radiative efficiency of all the metastable states, except for O(1S), is close to unity for radial distances above 10^3 km, where most of the emission intensity occurs. Since the emission intensity in the observed spectra is mostly determined by the radiative decay of the excited species, we can neglect the contribution of collisional broadening while converting the line width to the mean velocity of the excited species.

The line widths reported in Table 3 show that the atomic oxygen green line is broader than the red-doublet lines, and this is also consistent with the observation made in other comets (Cochran 2008; Decock et al. 2013, 2015). This can be explained by the excess velocity of oxygen atom acquired during the CO₂ photodissociation. The formation of O(1S) via CO₂ dissociative excitation occurs at shorter wavelengths compared to that of O(1D), which leads to more excess energy release and results in higher mean velocity. Raghuram & Bhardwa (2013) calculated the mean excess energy profiles of O(1S) and O(1D) in comet Hale-Bopp and showed that the photodissociative excitation reactions produce O(1S) with excess energies larger than for O(1D). Based on the measured line widths, Cochran (2008) suggested that the larger green line width could be due to the involvement of different energetic photons in dissociating a single parent species and/or dissociation of multiple species, producing O(1S) and O(1D) with different excess energies. Our model calculations suggest that CO₂ mainly produces both green and red-doublet emission lines and the involvement of other species is small (see Fig. 3). Hence, we argue that the observed green line width is larger than the red-doublet widths mainly because CO₂ is dissociated by high energetic solar photons which produce O(1S) with large excess velocities.
Similarly, the width of $[\text{CI}]$ 8727 Å line is larger than that of 9850 Å line and can also be due to the involvement of high energetic photons in the photodissociation of CO. The dissociation thresholds of CO producing $\text{C}^1(\text{D})$ and $\text{C}^1(\text{S})$ are 12 and 14 eV, respectively. Hence, the CO dissociation by high energetic photons leads to more excess velocity for $\text{C}^1(\text{S})$ than for $\text{C}^1(\text{D})$. Moreover, the production rate of atomic carbon via CO dissociative excitation is very low compared to that of CO (Huebner et al. 1992). Hence, the role of CO in the $\text{C}^1(\text{S})$ formation can be neglected. As shown in Fig. [1], the radiative decay of $\text{C}^1(\text{P})$ can also populate $\text{C}^1(\text{D})$, which additionally contribute to the emission intensities at wavelengths 9824 and 9850 Å. Since this formation channel occurs at energies higher than 18 eV, where most of the CO turns into ion, the contribution from radiative decay of $\text{C}^1(\text{P})$ can be neglected in the formation of $\text{C}^1(\text{S})$.

Our observed red-doublet emissions' line widths are similar, which suggests that the $\text{O}^1(\text{D})$ is released with a mean excess velocity of 2.01 km/s from dissociative excitation (see Table 5). The derived line widths for the 5198 and 5200 Å emissions, which arise due to radiative decay of same excited state, i.e., $\text{N}^2(\text{D})$ (see Fig. [1], are compatible with the uncertainties in the observation.

5.6. On the doublet emission bands

The radiative decay of metastable states viz., $\text{C}^1(\text{D})$, $\text{O}^1(\text{D})$, and $\text{N}^2(\text{D})$ to the ground state produces doublet emissions due to splitting in the sub-levels of the electronic states (see Fig. [1]). Hence, the observed intensity ratio of these doublet emission lines should be equal to the ratio of the Einstein decay probability coefficients of the corresponding transitions. The $[\text{CI}]$ 9824 Å emission line is strongly contaminated by telluric absorption line which did not allow us to determine precisely the $[\text{CI}]$ 9824/9850 emission ratio. On the contrary the measured $[\text{OI}]$ ratio over the full slit is well determined and is in agreement with the theoretical value (Wiese et al. 1996). Based on the theoretical calculations of Tachiev & Froese Fischer (2002), Wiese & Fuhr (2007) recommend a transition probability ratio of the $\text{[NI]}$ doublet equal to 2.6. But our observations show that this value is $1.22 \pm 0.09$, which is nearly half the Wiese & Fuhr (2007) value. Sharpee et al. (2005) noticed that there is a significant difference between the calculated and observed $[\text{NI}]$ emission ratios. They measured the $[\text{NI}]$ emission ratio in the night glow of the terrestrial spectrum and found it has an average value of 1.76. In the terrestrial atmosphere, strong collisions between $\text{N}^2(\text{D})$ and other species can alter the statistical population of atomic nitrogen excited levels, which subsequently affects the intensity ratio of the $[\text{NI}]$ emission lines. The Hernandez & Turtle (1969) and Sivjee et al. (1981) measurements have shown that the $[\text{NI}]$ ratio varies between 1.2 and 1.9. Sivjee et al. (1981) calculated an emission ratio profile by considering major collisional quenching reactions of $\text{N}^2(\text{D})$. They found that $[\text{NI}]$ ratio can be as low as 1.1. Our calculated lifetime profiles show that throughout the coma, the $\text{N}^2(\text{D})$ density is essentially determined by transport rather than quenching due to the poor collisional interactions with other cometary species (see Fig. [5]). Hence, the role of collisional quenching in the observed $[\text{NI}]$ ratio can be neglected. Based on the observations and modelling, we argue that the measured $[\text{NI}]$ emission ratio is mainly due to the intrinsic transition probability ratio of sub-levels of $\text{N}^2(\text{D})$. As discussed in the earlier section, it is difficult to measure the $[\text{NI}]$ ratio experimentally due to the $\text{N}^2(\text{D})$ long lifetime (~10 hrs) while the collisional quenching in the terrestrial environment can alter the observed $[\text{NI}]$ ratio significantly. Hence, the cometary spectroscopic observations are a new natural way to explore atomic and molecular properties that can not be determined in the laboratory.

6. Summary and Conclusions

The recent observations of C/2016 R2 have shown that its coma has a peculiar composition compared to most comets observed so far. Several forbidden emission lines have been detected in the optical, some for the first time, using UVES mounted on the Very Large Telescope (Opitom et al. 2019). The observed atomic carbon, oxygen, and nitrogen forbidden emission transitions are modelled under the frame-work of a coupled-chemistry emission model, by incorporating the major production, loss, and transport mechanisms of $\text{C}^1(\text{D} \& \text{1} \text{S}), \text{O}^1(\text{D} \& \text{1} \text{S}),$ and $\text{N}^2(\text{D})$ species. The observation of these forbidden emissions in a water depleted comet is a first and unique case to study the photochemistry of the metastable states and their emission processes in such a cometary coma. The major conclusions drawn from both observations and modelling are as follows:

1. The major source of $[\text{OI}], [\text{CI}],$ and $[\text{NI}]$ emissions is found to be the photodissociation of $\text{CO}_2, \text{CO},$ and $\text{N}_2$, respectively.
2. The collisional quenching of all the metastable states, except for $\text{O}^1(\text{S})$ and $\text{C}^1(\text{S})$ is significant for radial distances below $3 \times 10^3$ km. The collisional quenching of $\text{C}^1(\text{D})$ and $\text{N}^2(\text{D})$ occurs mainly by CO whereas it is by CO$_2$ for $\text{O}^1(\text{D})$.
3. In this water depleted coma, the observed $[\text{OI}]$ G/R emission ratio is found to vary between 0.3 and 0.18, which is smaller than the Festou & Feldman (1981) value of 0.9 for a CO$_2$ coma by a factor of 3 or more. This lower value indicates that the observed $[\text{OI}]$ G/R emission ratio is not a parameter to identify the major parent source, neither water nor CO$_2$.
4. The observed width of the green emission line is larger mainly because of the photodissociation of CO$_2$ which occurs by high energetic photons, which results in $\text{O}^1(\text{S})$ having large excess mean velocity. Since the photodissociation of CO$_2$ is the only source of the oxygen emission lines, the involvement of multiple species in producing the larger green line width can be discarded in this comet.
5. By comparing the observed and modelled $[\text{CI}]/[\text{NI}]$ emission ratios in this comet, we suggest that the photodissociation cross section of CO producing $\text{C}^1(\text{D})$ should be reduced by a factor of 4.
6. Using a high molecular oxygen abundance (about 30% with respect to CO), our modelled $[\text{OI}]$ G/R ratio is consistent with the observations for radial distances below $10^3$ km. Above this radial distance, the modelled values are higher by 40% than the observations. This suggests that the photodissociation of molecular oxygen is a possible source of these emission lines.
7. Based on the observations and modelling of these emissions we suggest that in a water-depleted and CO$_2$ rich cometary coma, which could be the case for comets observed at large (>3 au) heliocentric distance as $\text{H}_2\text{O}$ is not sublimating yet, the observed $[\text{OI}]$ emissions are mainly governed by CO$_2$.
8. The modelling of the $[\text{OI}]$ G/R ratio suggests that the ratio of dissociation frequencies of CO$_2$ producing O$^1(\text{S})$ to O$^1(\text{D})$ should be around 0.2. Similarly, the modelled $[\text{CI}]/[\text{NI}]$ emission ratio suggests that mean branching fraction of CO for the production of $\text{C}^1(\text{D})$ should be smaller by a factor of 3 to 5 than the Huebner et al. (1992) values. The observed
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emission ratios of metastable species in the non-collisional region is a new way to constrain the mean branching ratio of metastable species produced via photodissociative excitation.

9. In spite of having a long radiative lifetime (~10 hrs), N(2D) is mainly controlled by transport rather than collisional quenching. Hence the observed [NI] ratio of 1.22, which is smaller than the terrestrial measurement by a factor of 0.7, is mainly due to the intrinsic transition probability ratio.

10. The simultaneous observation of both [CI] 8727 Å and 9850 Å emission lines allowed us to constrain the yield of CO photodissociation producing C(1S). It is about 1/5% of the total absorption cross section, which was not previously determined in the laboratory. This suggests that cometary spectroscopic observations serve as a natural laboratory to explore the atomic and molecular properties.

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