Power-Optimal Feedback-Based Random Spectrum Access for an Energy Harvesting Cognitive User

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Abstract—In this paper, we study and analyze cognitive radio networks in which secondary users (SUs) are equipped with Energy Harvesting (EH) capability. We design a random spectrum sensing and access protocol for the SU that exploits the primary link’s feedback and requires less average sensing time. Unlike previous works proposed earlier in literature, we do not assume perfect feedback. Instead, we take into account the more practical possibilities of overhearing unreliable feedback signals and accommodate spectrum sensing errors. Moreover, we assume an interference-based channel model where the receivers are equipped with multi-packet reception (MPR) capability. Furthermore, we perform power allocation at the SU with the objective of maximizing the secondary throughput under constraints that maintain certain quality-of-service (QoS) measures for the primary user (PU).

Index Terms—Energy harvesting, cognitive radio, feedback, quality-of-service, multi-packet.

1. INTRODUCTION

Cognitive radio is a promising technology that efficiently utilizes the radio spectrum [1]. Its essence resides in allowing secondary users (SUs) to access the spectrum while the primary users (PUs) are silent. Moreover, secondary nodes can use the spectrum concurrently with primary nodes in condition that they guarantee certain quality-of-service measures for the primary network.

Cognitive radio networks may involve some battery-based nodes and hence, energy management becomes a very important aspect. In many applications, the SU is a battery-constrained device. Therefore, its operation, which includes spectrum sensing and access, depends largely on its energy resources. Recently, energy harvesting has been gaining increasing worldwide interest. It is an emerging technology that is considered a promising solution to wireless energy-constrained networks. The significance of this technology resides in its capability to prolong wireless networks lifetime [2]. With such technology, nodes are capable of collecting energy from the surrounding environment [3].

Studying data transmission by an energy harvester with a rechargeable battery has received a lot of attention in the literature [5–12]. Using a dynamic programming framework, Lei et al. [5] derived the optimal online policy for controlling admissions into the data buffer. In [6], Sharma et al. investigate the energy management policies that stabilize the data queue of a single-user communication. The authors derive some delay-optimal properties. For energy harvesting systems in a time-constrained slotted setting, the authors in [7] discussed the throughput-optimal energy allocation. In [8, 9], Yang et al. minimize the transmission completion time of an energy harvesting system. The optimal solution is obtained using a geometric framework. In [10], the authors solve the problem of maximizing the amount of data transmitted in a finite time horizon. The network under consideration consists of energy harvesting transmitters with batteries of finite energy storage.

In the context of cognitive communications, the authors in [11] consider a simple network composed of one PU and one SU. The PU is assumed to be equipped with a rechargeable battery (energy queue with random arrivals). The energy queue is assumed to be modelled as a decoupled M/D/1 queue with Bernoulli arrivals and unity service rate. The SU is plugged to a reliable power supply; it always has energy/power. The maximum stable throughput region was derived using the dominant system approach [13].

The optimal sensing and access policies for an energy harvesting SU based on Markov decision processes (MDPs) have been investigated in [14]. In [15], the optimal sensing duration of an energy harvesting SU is selected randomly at the beginning of every time slot from a predetermined set. The stable throughput is obtained via optimizing over the possibility of choosing certain sensing durations.

Due to the broadcast nature of wireless channels, primary feedback can be overhead by all nodes in the network. The main problem with schemes that employ spectrum sensing only is that sensing does not inform the SU about the impact of its transmissions on the primary receiver. This issue induced interest in leveraging the feedback sent by the primary receiver at the end of time slots to the primary transmitter in order to optimize the secondary transmission strategies. In [16], Eswaran et al. assume that the SU observes the feedback from the primary receiver as it reflects the achieved primary rate. The SU aims at maximizing its throughput while guaranteeing a certain primary packet rate. The authors of [17] use a partially observable Markov decision process (POMDP) to optimize the secondary action using the spectrum sensing outcome and primary Automatic Repeat reQuest (ARQ) feedback.
Section II. System Model

We consider the cognitive radio system shown in Fig. 1. The system consists of a PU (p) transmitting its packets to a primary destination (d_p). In addition, there exists an SU (s) communicating with a secondary destination (d_s). The PU is plugged to a reliable power supply. This means that it never lacks energy/power. However, the SU is equipped with a rechargeable battery. We assume that the SU harvests energy from the surrounding environmental energy sources, e.g., solar energy, wind energy, etc. All nodes are equipped with infinite capacity buffers to store fixed-length (β bits) data packets. Time is slotted and the duration of one time slot is T seconds. The transmission of a packet takes one time slot.

The channel between every transmitter-receiver pair exhibits frequency-flat Rayleigh block fading, i.e., the channel coefficient remains constant for one time slot and changes independently from a slot to another. Moreover, a zero-mean additive white Gaussian noise of power spectral density N_0 Watts/Hz is taken into account. The channel coefficient between transmitter i and receiver j at the nth time slot is denoted by h_{ij}[n]. According to the Rayleigh fading assumption, h_{ij}[n] is a complex Gaussian zero-mean random variable with variance σ_{ij}^2, i.e., h_{ij}[n] ∼ CN(0, σ_{ij}^2). Therefore, |h_{ij}[n]|^2 is exponentially-distributed with rate 1/σ_{ij}^2, i.e., |h_{ij}[n]|^2 ∼ exp(1/σ_{ij}^2). All links are considered statistically independent.

Instead of assuming a simple packet-erasure model, we consider simultaneous multi-packet transmission capability. This opens room for both the PU and SU to use the spectrum concurrently. Assuming that the receivers are equipped with multi-packet reception (MPR) capability, transmitted data packets can survive the interference caused by concurrent transmissions if the received signal-to-interference-and-noise ratio (SINR) exceeds the threshold required for successful decoding. The SU performs probabilistic spectrum sensing. We take into account erroneous spectrum sensing outcomes.

Next, we present the queueing model of the system followed by the description of the proposed spectrum access protocol.

A. Queueing Model

The queues involved in system analysis, shown in Fig. 1, are described as follows:
- Q_p: stores the data packets of the PU.
- Q_s: stores the data packets of the SU.
- Q_e: stores the harvested energy at the SU.

The bursty nature of information sources is taken into account through modelling the data arrivals at the PU as a Bernoulli process with rate λ_p (packets/slot). In other words, at any given time slot, a packet arrives at the PU with probability λ_p < 1. On the other hand, we assume that Q_s is backlogged, i.e., the SU always has packets awaiting transmission to d_s. The arrivals at the energy queue are assumed to follow a stationary Poisson process with rate λ_e. This captures the random availability of ambient energy sources. The arrival processes at Q_p and Q_s are independent of each other, and are independent and identically-distributed (i.i.d) across time slots. Upon successful reception of a primary packet, d_p broadcasts an acknowledgement (ACK). However, if d_p fails to decode a primary packet, it broadcasts a negative-acknowledgement (NACK). ACKs and NACKs are assumed instantaneous and can be heard by the PU and SU. The PU receives the feedback sent by d_s reliably with probability 1. On the contrary, the SU overhears reliable primary feedback with probability q.

The instantaneous evolution of queue lengths is captured as

\[ Q_i[n+1] = (Q_i[n] - L_i[n])^+ + A_i[n], \quad i \in \{p, s\} \]  \hspace{1cm} (1)

where \((z)^+ = \max(z, 0)\) and \(Q_i[n]\) denotes the number of packets in the ith queue at the beginning of the nth time slot. \(L_i[n]\) and \(A_i[n]\) denote the departures and arrivals corresponding to the ith queue in the nth time slot, respectively.

B. Spectrum Access Protocol

Whenever \(Q_p\) is non-empty, the PU transmits a packet with average power \(P_p\). However, the SU probably attempts to transmit the head-of-line packet in its data queue if its battery
has got the energy required to support that transmission. The spectrum access protocol employed at the SU exploits the available primary feedback signals. The SU may overhear nothing if there is no primary transmission. However, it may overhear an ACK or a NACK if the primary receiver correctly decodes, or fails to decode, the primary transmission, respectively, while the SU decodes the feedback signals correctly. Otherwise, the SU may overhear un-decodable feedback signals. Given that a primary transmission takes place in a given time slot, the SU is capable of decoding the primary feedback signals with probability \( g \) as indicated earlier. If the SU receives nothing, an ACK or un-decodable feedback, it gains no information about the PU’s activity in the next time slot. Therefore, the SU operates as follows:

- If the energy required for transmission is available at \( Q_s \), it performs spectrum sensing with probability \( \alpha_s \) from the beginning of the time slot for a duration \( \tau < T \) seconds to detect the possible activity of the PU.
- The SU transmits with probability \( \alpha_f \) or \( \alpha_b \) if the PU is detected to be idle or busy, respectively.
- At the beginning of the time slot, if the SU decides not to sense the spectrum (which happens with probability \( 1 - \alpha_s \)), it immediately decides whether to transmit with probability \( \alpha_s \) or to remain idle for the rest of the time slot with probability \( 1 - \alpha_s \).

Whenever the SU transmits in these cases, it uses an average power \( P_s^{(1)} \) when the PU is sensed to be inactive; and \( P_s^{(2)} \) when the PU is sensed to be active. Note that \( P_s^{(2)} \) should be lower than \( P_s^{(1)} \) to reduce the expected interference on the primary transmission. On the other hand, if a NACK is overheard by the SU, it knows that the PU will retransmit the lost packet during the next time slot with probability \( 1 \). Being sure that the PU is active in the next slot, the SU does not need to perform spectrum sensing. Therefore, it accesses the channel from the beginning of the time slot with probability \( \alpha_f \). In that case, the SU transmits with average power \( P_s^{(3)} \leq P_s^{(2)} \leq P_s^{(1)} \) to reduce its interference to the primary receiver.

\[\begin{align*}
\text{Fig. 1: Cognitive radio network under consideration.}
\end{align*}\]

We assume that energy dissipation from \( Q_s \) happens when the SU transmits data. The energy consumed in spectrum sensing and primary feedback decoding is negligible and out of the scope of this paper.

**III. PERFORMANCE ANALYSIS**

In this section, we provide the queueing analysis of the proposed access scheme. In particular, we derive stability conditions on the queues involved in the system. The system is considered stable when all of its queues are stable. Queue stability is loosely defined as having a bounded queue size, i.e., the number of packets in the queue does not grow to infinity as time progresses [21]. Furthermore, we provide a closed-form expression for the average primary packet delay.

**A. Queueing Analysis**

The PU’s queue-length evolution Markov chain (MC) is shown in Fig. 2. We refer to the probability of the queue having \( k \) packets and transmitting for the first time as \( \pi_k \), where \( F \) in Fig. 2 denotes the first transmission. The probability of the queue having \( k \) packets and retransmitting is \( \gamma_k \), where \( R \) in Fig. 2 denotes retransmission. The probability of successful transmission of a PU’s packet in case of first transmission and a retransmission is given by \( \Omega_p \) and \( \Gamma_p \), respectively. We proceed with calculating these probabilities.

\[\begin{align*}
\Omega_p &= \mathbb{P} \gamma + \mathbb{P} P_0(P_p, 0) \\
\end{align*}\]

where \( \mathbb{P} \) is the probability that \( Q_s \) has got the amount of energy sufficient for one secondary packet transmission, \( P_0(P_A, P_{\text{II}}) \) is derived in the Appendix and \( \gamma \) is given by

\[\begin{align*}
\gamma &= \alpha_f \mathbb{P} P_0(P_p, P_s^{(1)}) + \alpha_b \mathbb{P} P_0(P_p, 0) \\
&+ \alpha_f \mathbb{P}_{\text{MD}} \left\{ \alpha_s \mathbb{P} P_0(P_p, P_s^{(1)}) + \alpha_f \mathbb{P} P_0(P_p, 0) \right\} \\
&+ \alpha_f \mathbb{P}_{\text{MD}} \left\{ \alpha_b \mathbb{P} P_0(P_p, P_s^{(2)}) + \alpha_b \mathbb{P} P_0(P_p, 0) \right\}.
\end{align*}\]

State-self transitions are not depicted on the graph for visual clarity. Throughout the paper, \( \mathbb{P} = 1 - \gamma \).
We denote the probability of miss-detection by $P_{MD}$. On the other hand, it can be shown that $\Gamma_p$ is given by

$$
\Gamma_p = \mathbb{P} \left[ q \left( \alpha_r P_0(P_p, P_s^{(3)}) + \Pi P_0(P_p, 0) \right) + \overline{\gamma} \right] + \mathbb{P} P_0(P_p, 0). \tag{4}
$$

We solve for the steady-state distribution of the PU’s MC. Solving the state balance equations of the MC depicted in Fig. 3, we obtain the state probabilities which are provided in Table 1. The probability $\pi_0$ is obtained using the normalization condition $\sum_{k=0}^{\infty} (\pi_k + \chi_k) = 1$. It should be noticed that $\lambda_p \leq \eta$, where $\eta$ is defined in Table 1 is a condition for the sum $\sum_{k=0}^{\infty} (\pi_k + \chi_k)$ to exist. This condition ensures the existence of a stationary distribution for the MC. Furthermore, it guarantees the stability of $Q_p$, i.e., $Q_p$ has a non-zero probability of being empty ($\eta_0 > 0$).

From (2) and (4), we notice that $\Omega_p$ and $\Gamma_p$ depend on the state of $Q_e$ through the term $P$. Therefore, we need to model the energy dissipation from the battery of the SU, i.e., $Q_e$. Let $P_{FA}$ denote the probability of false alarm. According to the proposed access protocol described in Section IV-B, the mean service rate of $Q_e$ is given in (5) at the top of the following page.

It is obvious that the service rate of $Q_e$ depends on the state of $Q_p$, i.e., $\pi_k$ and $\chi_k$. Thus, $Q_p$ and $Q_e$ are two interacting queues. The relaxation of this interaction and the computation of $\mathbb{P}$ is provided in the next section.

We proceed next with characterizing the SU throughput, i.e., the mean service rate of $Q_e$. It is given in (6) at the top of the following page. The dependence of the SU throughput on both $Q_e$ and $Q_p$ is highlighted in (6). The SU transmits only when the energy required to support its transmission is available in $Q_e$. This explains the role of $\mathbb{P}$ in (6). In addition, the SU’s behavior depends on the state of the PU, i.e., the PU being in a first transmission or a retransmission state. By behavior here we refer to the decisions made by the SU concerning spectrum sensing and access and the choice of transmission powers.

### B. Average Primary Packet Delay

Applying Little’s law (22), we obtain a closed-form expression for the average primary packet delay, which is given by

$$
D_p = \frac{1}{\lambda_p} \sum_{k=1}^{\infty} k (\pi_k + \chi_k). \tag{7}
$$

Using the state probabilities provided in Table 1

$$
D_p = \frac{(\Omega_p - \eta)(\eta - \lambda_p)^2 + (1 - \lambda_p)^2 (1 - \Omega_p) \eta}{(\eta - \lambda_p)(1 - \lambda_p)(1 - \eta) \Gamma_p}. \tag{8}
$$

### IV. Bounds on Secondary Throughput and Problem Formulation

In this section, we derive lower and upper bounds on the throughput of the SU. Our main goal now is to relax the interaction between $Q_e$ and $Q_p$ to be able to compute $\mathbb{P}$ and $\{\pi_k, \chi_k\}_{k=0}^{\infty}$ and hence, the throughput of the SU can be characterized.

### A. Lower Bound on $\mu_s$

We analyze the effect of the states of $Q_p$ and $Q_e$ on the SU throughput. We begin first with $Q_p$. If the PU’s service rate is decreased, less number of packets probably depart $Q_p$. This implies that the probability of $Q_p$ being empty is lowered. Therefore, the PU is more likely to be active and hence, the interference on the SU is increased which lowers its throughput. This motivates us to derive lower bounds on $\Omega_p$ and $\Gamma_p$ provided in (3) and (4), respectively. We note that the worst case scenario with respect to the PU occurs when it experiences continuous possible interference from the SU. Since the SU is assumed backlogged, continuous SU transmission possibly occurs when it always has the required energy, i.e., $\mathbb{P} = 1$. Substituting by $\mathbb{P} = 1$ in (2) and (4),

$$
\Omega_p \geq \gamma \tag{9}
$$

$$
\Gamma_p \geq q \left\{ \alpha_r P_0(P_p, P_s^{(3)}) + \Pi P_0(P_p, 0) \right\} + \overline{\gamma} \tag{10}
$$

where $\gamma$ is given by (3).

On the other hand, we note from (5) that the energy dissipation from $Q_e$, whenever a secondary transmission occurs, is one of four levels: (i) $P_s^{(1)} T_s$, (ii) $P_s^{(1)} T_s$, (iii) $P_s^{(2)} T_s$ and (iii) $P_s^{(3)} T$. We assume that $Q_e$ dissipates $P_s^{(1)} T$ for each secondary transmission provided that this energy is available in $Q_e$. This provides an upper bound on the service rate of $Q_e$ because $P_s^{(1)} T$ is the one which has the highest level among the aforementioned four levels. Hence, the SU battery is depleted faster which negatively impacts its throughput. This assumption renders $Q_e$ an M/D/1 queue with arrival rate $\lambda_e$. 

| $\eta$ | $\lambda_p \Omega_p + (1 - \lambda_p) \Gamma_p$ |
| $\pi_0$ | $\frac{\eta - \lambda_p}{\lambda_p}$ |
| $\chi_0$ | 0 |
| $\pi_1$ | $\pi_0 \lambda_p \frac{\lambda_p+(1-\lambda_p) \Gamma_p}{\eta}$ |
| $\chi_1$ | $\pi_0 \lambda_p \frac{\lambda_p+(1-\lambda_p) \Gamma_p}{\eta}$ |
| $\pi_k$, $k \geq 2$ | $\pi_0 \lambda_p \left( \frac{\lambda_p \Gamma_p}{\eta - \lambda_p} \right)^k$ |
| $\chi_k$, $k \geq 2$ | $\pi_0 \lambda_p \left( \frac{\lambda_p \Gamma_p}{\eta - \lambda_p} \right)^k$ |
| $\sum_{k=1}^{\infty} \pi_k$ | $\pi_0 \lambda_p \frac{\Gamma_p}{\eta - \lambda_p} = \lambda_p$ |
| $\sum_{k=1}^{\infty} \chi_k$ | $\pi_0 \lambda_p \frac{\Gamma_p}{\eta - \lambda_p} (1 - \Omega_p) = \frac{\lambda_p}{\lambda_p} (1 - \Omega_p)$ |

TABLE I: Steady-state distribution for the PU’s MC.
and service rate $P_0^{(1)}T$. Therefore, $P$ is

$$P = \min \left[ 1, \frac{\lambda_e}{P_0^{(1)}T} \right].$$

We use the lower bounds on $\Omega_p$ and $\Gamma_p$ provided on the right hand sides of (9) and (10), respectively, to compute the state probabilities of the PU’s MC given by Table I. Substituting by these state probabilities along with $P$ as given by (11) in (6), we get a lower bound on the throughput of the SU.

**B. Upper Bound on $\mu_s$**

We use a similar approach to the one presented in Section IV-A to derive an upper bound on the SU throughput. When the service rate of the PU’s queue increases, this increases the availability of time slots in which the PU is silent. Thus, the interference on the SU decreases and its throughput is enhanced. This motivates us to derive upper bounds on $\Omega_p$ and $\Gamma_p$. The best case scenario with respect to the PU occurs when it experiences no interference from the SU, as if the SU does not exist. This happens when the battery of the SU is always empty, corresponding to $P = 0$. Substituting by $P = 0$ in (2) and (4), we get

$$\Omega_p \leq P_0(P_p, 0)$$

$$\Gamma_p \leq P_0(P_p, 0).$$

On the other hand, we assume that $Q_e$ dissipates $\min[P_0^{(2)}T_s, P_0^{(3)}T_s]$ for each secondary transmission provided that this energy is available in $Q_e$. This provides a lower bound on the service rate of $Q_e$. Hence, the SU battery lifetime increases which positively impacts its throughput. This assumption renders $Q_e$ an M/D/1 queue with arrival rate $\lambda_e$ and service rate $\min[P_0^{(2)}T_s, P_0^{(3)}T_s]$. Therefore, $P$ is given by (12)

$$P = \min \left[ 1, \frac{\lambda_e}{\min[P_0^{(2)}T_s, P_0^{(3)}T_s]} \right].$$

We use the upper bounds on $\Omega_p$ and $\Gamma_p$ provided on the right hand sides of (12) and (13), respectively, to compute the state probabilities of the PU’s MC given by Table I

$$\mu_s = \mathbb{P} \left[ \pi_0 \left\{ \Gamma_0, P_0^{(1)}, P_0^{(2)} + \sum_{k=1}^{\infty} \chi_k \left\{ q_0, P_0^{(3)}, 0 \right\} \right\} \right].$$

Substituting by these state probabilities along with $P$ as given by (14) in (6), we get an upper bound on the SU throughput.

**C. Problem Formulation**

Using the relevant mean service rates under each of the proposed bounds, for a fixed $\lambda_p$, the following constrained optimization problem is solved numerically

$$\begin{align*}
&\text{maximize} & & \mu_s \\
&\text{subject to} & & 0 \leq \alpha_s, \alpha_t, \alpha_b, \alpha_r, \alpha_t, \alpha_r \leq 1 \\
& & & 0 \leq P_0^{(1)} < P_0^{(2)} < P_0^{(3)} \leq P_0 \\
& & & \lambda_p \leq \eta \\
& & & D_p \leq D_o.
\end{align*}$$

We set maximum secondary transmission power constraint $P_0$, and a threshold $D_o$ below which the average primary packet delay is kept. Note that the optimization problem is solved at the secondary terminal. We use MatLab’s fmincon to solve the optimization problems as in [19], [23]–[26] and the references therein.

**V. NUMERICAL RESULTS**

In this section, the performance of the proposed scheme is evaluated in terms of the SU throughput. We formulate and solve an optimization problem with the objective of maximizing the secondary throughput subject to certain guaranteed QoS measures for the PU. We solve for the optimal sensing and access probabilities as well as the average secondary transmission powers that maximize the SU throughput while simultaneously keeping the PU’s queue stable and the primary packet delay below a certain threshold.

We show our results for packet-length $\beta = 10$ bits, time slot duration $T = 1$ second and sensing duration $\tau = 0.3$ second. Sensing errors are taken into account through setting $P_{MD} = P_{FA} = 0.3$. All links are considered statistically equivalent where $\alpha_i^2 = 1 \forall i \in \{p, s\}$ and $j \in \{d_p, d_s\}$. The bandwidth of these channels is set to $W = 8$ Hz. The PU transmits its packets with average power $P_0 = 20$ Watts. The power spectral density of noise is normalized to unity, i.e., $N_0 =$...
the outer bound decreases with the increase of \( \lambda_e \). From the figure, we note that the gap between the inner and outer bounds decreases as \( \lambda_e \) increases. This is attributed to the fact that the restriction on the SU’s activity originating from its energy resources is relaxed as \( \lambda_e \) increases. From the figure, we note that the gap between the inner and the outer bound decreases with the increase of \( \lambda_e \).

Next, we depict the effect of unreliable primary feedback signals on SU throughput and average primary packet delay. Towards this objective, we plot the optimal lower bound on \( \mu_s \) versus \( \lambda_p \) for different values of \( q \) in Fig. 4. We choose \( \lambda_e = 20 \) and \( D_o = 10 \) time slots. As shown in the figure, the throughput of the SU is enhanced as \( q \) increases. This shows that the best case scenario occurs when the SU receives perfect primary feedback, i.e., \( q = 1 \). However, the worst case scenario occurs when the SU overhears no reliable feedback from the PU, i.e., \( q = 0 \). The case of \( q = 0 \) boils down to the case in which the SU can not overhear/decode the primary feedback signals. On the other hand, we evaluate the underlying average PU delay. We use the resulting optimal sensing and access probabilities as well as average secondary transmission powers, used to plot Fig. 5 in computing the average primary packet delay given by (3). It is worth noting that the primary delay computed through solving (15) with the objective of maximizing the lower bound on \( \mu_s \) is an upper bound on the achievable PU delay. In Fig. 5 we plot the PU’s delay versus \( q \) at selected values of \( \lambda_p \). Thus, it can be seen that the primary delay is a decreasing function of \( q \). Therefore, we reach the conclusion that reliable feedback signals overheard by the SU is not only in its interest, but it also enhances the PU’s performance.

Furthermore, we investigate the effect of the QoS measures guaranteed for the PU on the throughput of the SU. Specifically, we depict the effect of varying the average primary queueing delay constraint on the SU throughput in Fig. 6. The results are plotted for \( q = 0.8 \) and \( \lambda_e = 20 \) energy packets/slot. From Fig. 6 we note that the lower bound on SU throughput is enhanced as the primary delay constraint is relaxed, i.e., \( D_o \) is increased. This intuitive result is attributed to the fact that for a less restrictive primary delay constraint, the feasible set of the optimization variables is widened. Thus, we are able to achieve better SU throughput at higher values of \( D_o \).

In Fig. 5 we show the essence of performing power allocation at the SU. We plot the resulting optimal lower bound on \( \mu_s \) with and without optimizing over the powers \( P_s^{(1)} \), \( P_s^{(2)} \) and \( P_s^{(3)} \). In the latter case, we set \( P_s^{(1)} \), \( P_s^{(2)} \) and \( P_s^{(3)} \) to zero. Towards this objective, we plot the optimal lower bound on \( \mu_s \) versus \( \lambda_p \) for different values of \( q \) in Fig. 7. We choose \( \lambda_e = 20 \) and \( D_o = 10 \) time slots. As expected, the figure shows that the SU throughput is enhanced as \( \lambda_e \) increases. This is attributed to the fact that the restriction on the SU’s activity originating from its energy resources is relaxed as \( \lambda_e \) increases. From the figure, we note that the gap between the inner and the outer bound decreases with the increase of \( \lambda_e \).
and $P_s^{(3)}$ to their maximum possible value, i.e., $P_e$. We set $\lambda_p = 20$ energy packets/slot and $q = 0.8$. From the figure, we note that the SU throughput is enhanced when we optimize over the transmission powers and the resulting optimal values for $P_s^{(1)}$, $P_s^{(2)}$, and $P_s^{(3)}$ is definitely less than $P_e$. Thus, we achieve higher SU throughput at lower average power consumption. We note that at $\lambda_p = 0.3759$ packets/slot, the problem becomes infeasible and there are no optimization variables would satisfy the primary constraints. Hence, the SU remains silent and it gains no access to the channel.

VI. CONCLUSION

We propose a novel random spectrum sensing and access scheme for a cognitive radio SU equipped with energy harvesting capability. The cognitive user utilizes the primary feedback signals to decide on its spectrum sensing and access probabilities. Furthermore, we optimize over the SU’s transmission power with the objective of maximizing its throughput while simultaneously keeping the primary queue stable, and its average delay below a certain threshold. We investigate the effect of erroneous primary feedback signals overhead by the SU. We show that reliable feedback is in the interest of both the PU and SU. Moreover, we show the essence of performing power allocation at the SU compared to schemes in which SUs transmit with their maximum permissible power.

APPENDIX

We derive the probability of successful transmission in the presence of interference. Consider two nodes, A and B, transmitting to a common destination, d, with average powers $P_A$ and $P_B$, respectively. With respect to d, node A’s transmission is the intended signal, while node B is considered an interferer. In a given time slot, A transmits one packet ($\beta$ bits). The transmission duration is either $T - \tau$ or $T$ (seconds) depending on whether the transmission is preceded by a sensing phase or not, respectively. Thus, the transmission rate is given by

$$r_i = \frac{\beta}{T - i\tau}, \ i \in \{0, 1\}. \quad (16)$$

Consequently, we use the notion of channel outage to write the probability of success on the link $A \rightarrow d$ as

$$P_s(P_A, P_B) = \Pr \left\{ W \log \left( \frac{P_A|h_{A,d}|^2}{N_0W + P_B|h_{B,d}|^2} \right) > r_i \right\} \quad (17)$$

where $W$ is the channel bandwidth and $\Pr(E)$ denotes the probability of event $E$. After some algebraic manipulation,

$$P_s(P_A, P_B) = \Pr \left\{ \frac{|h_{A,d}|^2}{P_A/(N_0W)} + \frac{(2|\mathbb{E}| - 1)P_B}{P_A}|h_{B,d}|^2 \right\} \quad (18)$$

For the sake of exposition, let $a = \frac{1 - \epsilon}{P_A/(N_0W)}$, $b = \frac{(2|\mathbb{E}| - 1)P_B}{P_A}$ and $X = |h_{B,d}|^2$. Thus, we have

$$P_s(P_A, P_B) = \Pr \left\{ |h_{A,d}|^2 > a + bX \right\}. \quad (19)$$

Using total probability theory, [22] can be written as

$$P_s(P_A, P_B) = \int_0^\infty \Pr \left\{ |h_{A,d}|^2 > a + bX \right\} f_X(x) dx \quad (20)$$

where $f_X(.)$ denotes the probability density function (PDF) of $X$. Following the channel model described in Section II $|h_{A,d}|^2 \sim \exp(1/\sigma_{A,d}^2)$ and $X \sim \exp(1/\sigma_{B,d}^2)$. Therefore,

$$\Pr \left\{ |h_{A,d}|^2 > a + bX \right\} = e^{-(a+bx)/\sigma_{A,d}^2} \quad (21)$$

$$f_X(x) = \frac{1}{\sigma_{B,d}^2} e^{-x/\sigma_{B,d}^2}. \quad (22)$$

Substituting by (21) and (22) in (20) and solving the integral, the probability of success on the link $A \rightarrow d$ in the presence of an interferer (B) is given by

$$P_s(P_A, P_B) = \frac{\sigma_{A,d}^2 e^{-a/\sigma_{A,d}^2}}{\sigma_{A,d}^2 + b \sigma_{B,d}^2}. \quad (23)$$

REFERENCES

[1] Q. Zhao and B. Sadler, “A survey of dynamic spectrum access,” IEEE Signal Processing Magazine, vol. 24, no. 3, pp. 79–89, 2007.
[2] Z. Ding, I. Krikidis, B. Sharif, and H. V. Poor, “Wireless information and power transfer in cooperative networks with spatially random relays,” Available [Online]:http://arxiv.org/abs/1403.6164.pdf, 2014.

[3] H. Chen, Y. Li, J. L. Rebelatto, B. F. Uchoa-Filhoand, and B. Vucetic, “Harvest-then-cooperative Wireless-powered cooperative communications.” Available [Online]:http://arxiv.org/abs/1404.4120.pdf, 2014.

[4] S. Sudevalayam and P. Kulkarni, “Energy harvesting sensor nodes: Survey and implications,” IEEE Communications Surveys and Tutorials, vol. 13, no. 3, pp. 443–461, 2011.

[5] J. Lei, R. Yates, and L. Greenstein, “A generic model for optimizing single-hop transmission policy of replenishable sensors,” IEEE Transactions on Wireless Communications, vol. 8, no. 2, pp. 547–551, 2009.

[6] V. Sharma, U. Mukherji, V. Joseph, and S. Gupta, “Optimal energy management policies for energy harvesting sensor nodes,” IEEE Transactions on Wireless Communications, vol. 9, no. 4, pp. 1326–1336, 2010.

[7] C. Ho and R. Zhang, “Optimal energy allocation for wireless communications powered by energy harvesters,” in IEEE International Symposium on Information Theory (ISIT), Jun. 2010, pp. 2368–2372.

[8] J. Yang and S. Ulukus, “Transmission completion time minimization in an energy harvesting system,” in 44th Annual Conference on Information Sciences and Systems (CISS), March 2010, pp. 1–6.

[9] ——, “Optimal packet scheduling in an energy harvesting communication system,” IEEE Transactions on Communications, vol. 60, no. 1, pp. 220–230, Jan. 2012.

[10] K. Tutuncuoglu and A. Yener, “Optimum transmission policies for battery limited energy harvesting nodes,” IEEE Transactions on Wireless Communications, vol. 11, no. 3, pp. 1180–1189, March 2012.

[11] N. Pappas, J. Jeon, A. Ephremides, and A. Traganitis, “Optimal utilization of a cognitive shared channel with a rechargeable primary source node,” in Journal of Communications and Networks (JCN), vol. 14, no. 2, Apr. 2012, pp. 162–168.

[12] I. Krikidis, T. Charalambous, and J. Thompson, “Stability analysis and power optimization for energy harvesting cooperative networks,” IEEE Signal Processing Letters, vol. 19, no. 1, pp. 20–23, January 2012.

[13] R. R. Rao and A. Ephremides, “On the stability of interacting queues in a multiple-access system,” IEEE Transactions on Information Theory, vol. 34, no. 5, pp. 918–930, 1988.

[14] A. Sultan, “Sensing and transmit energy optimization for an energy harvesting cognitive radio,” IEEE wireless communications letters, vol. 1, no. 5, pp. 500–503, Oct. 2012.

[15] A. El Shafie and A. Sultan, “Optimal selection of spectrum sensing duration for an energy harvesting cognitive radio,” in GLOBECOM, 2013, pp. 1020–1025.

[16] K. Eswaran, M. Gastpar, and K. Ramchandran, “Bits through ARQs: Spectrum sharing with a primary packet system,” in IEEE International Symposium on Information Theory (ISIT), June 2007, pp. 2171–2175.

[17] F. Lapiccirella, Z. Ding, and X. Liu, “Cognitive spectrum access control based on intrinsic primary ARQ information,” in IEEE ICC, May 2010.

[18] S. Huang, X. Liu, and Z. Ding, “Distributed power control for cognitive user access based on primary link control feedback,” in IEEE INFOCOM, March 2010.

[19] A. El Shafie and A. Sultan, “Optimal random access and random spectrum sensing for an energy harvesting cognitive radio,” in IEEE 8th International Conference on Wireless and Mobile Computing, Networking and Communications (WiMob), 2012, pp. 403–410.

[20] A. El Shafie and A. Sultan, “Optimal random access for a cognitive radio terminal with energy harvesting capability,” IEEE Communications Letters, vol. 17, no. 6, pp. 1128–1131, 2013.

[21] A. Sadek, K. Liu, and A. Ephremides, “Cognitive multiple access via cooperation: protocol design and performance analysis,” IEEE Transactions on Information Theory, vol. 53, no. 10, pp. 3677–3696, Oct. 2007.

[22] D. P. Bertsekas, R. G. Gallager, and P. Humblet, Data networks. Prentice-Hall International, 1992, vol. 2.

[23] C. Lee, E. Irwin, and C. Hardy, “Polarization sensitive direction of arrival distribution for radio wave multipaths: A comparison of multiple geometric models,” IEEE Trans. Antennas and Propagat., vol. 61, no. 10, pp. 5355–5358, 2013.

[24] A. Bornschlegl, J. Pelle, S. Harmand, A. Faquelle, and J.-P. Corriou, “Thermal optimization of a high-power salient-pole electrical machine,” IEEE Trans. Industr. Electr., vol. 60, no. 5, pp. 1734–1746, 2013.

[25] S. Yin, S. Chan, and K. M. Tsui, “On the design of nearly-pr and pr fir cosine modulated filter banks having approximate cosine-rolloff transition band,” IEEE Trans. Circuits and Systems II: Express Briefs, vol. 55, no. 6, pp. 571–575, 2008.

[26] J. Gillet, M. David, and F. Messine, “Optimization of the control of a doubly fed induction machine,” in Proc. IEEE 11th International Workshop of Electronics, Control, Measurement, Signals and their Application to Mechatronics (ECMSM), 2013, pp. 1–5.