Efficient Up-Conversion ZnO Co-Doped (Er, Yb) Nanopowders Synthesized via the Sol-Gel Process for Photovoltaic Applications

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Abstract: In this study, undoped and (Erbium, Ytterbium) co-doped ZnO nanopowders were prepared using the sol-gel method and the supercritical drying of ethyl alcohol. Doping ZnO nanopowders were elaborated with 5 mol% of Er (5 Er: ZnO), 5 mol% of Er and 5 mol% of Yb (5 Er, 5 Yb: ZnO), and 5 mol% of Er and 10 mol% of Yb (5 Er, 10 Yb: ZnO) concentrations. The effects of the Yb concentration on the structural, morphological, photoluminescent, and electrical properties of the ZnO nanopowders were investigated. The main findings of this work were the crystallization of all of the nanopowders in a hexagonal Wurtzite structure with a spheroidal morphology and a size of 60 nm. Hence, the doping concentration would affect the crystallinity and the morphology of the ZnO nanopowder. The UC (Up-Conversion) emissions were investigated under a 980 nm excitation. It was observed that (Er, Yb: ZnO) exhibited green, ranging between 525 nm and 550 nm and red up-converted emissions of 655 nm, due to the efficient energy transfer process between Er$^{3+}$ and Yb$^{3+}$. The absolute quantum yield percentage (QY %) of the doped nanopowders was measured as a function of power density at each up-converted emission. This would prove that (5 Er, 5 Yb: ZnO) had the highest QY percentage value of 6.31 ± 0.2% at a power density of 15.7 W/cm$^2$. Additionally, it had the highest excited state lifetime for green and red emissions. Moreover, the Hall effect measures showed that the resistivity decreased while the electron mobility increased after doping, suggesting that most of rare earth ions were located in the interstitial positions. The carrier concentration increased after doping until (5 Er, 5 Yb: ZnO), suggesting that the Zn$^{2+}$ ions substituted the RE$^{3+}$ ions. Then, the carrier concentration decreased, suggesting that doping with higher concentrations would cause grain boundary defects. These findings would suggest that (5 Er, 5 Yb: ZnO) would have the best electrical properties and the lowest band gap energy (3.24 eV). Therefore, the presented preparation of the (Er, Yb: ZnO) nanopowders elaborated, using the sol-gel process would be a potential interesting material for UC applications.

Keywords: sol-gel processes; up-conversion luminescence; ZnO; rare earth materials

1. Introduction

It has been established that the inability of Si photovoltaic cells to absorb low energy was one of the main shortcomings of these photovoltaic devices [1]. In this context, the up-conversion process is one of the proposed solutions to modify the incident solar radiation [2]. In up-conversion (UC), a high-energy photon is generated from the exploitation of energy by two or multiple low-energy incident photons [3]. In this context, the rare earth doped oxide type materials are good candidates for UC convertors in the back of the Si solar cell panel [4]. The low cost, non-toxicity, high thermal and chemical stability, high resistance, optical transparency, piezoelectric properties, and other properties of zinc oxide (ZnO) semiconductors make it a suitable host matrix for doping rare earth elements [5]. ZnO has a large band gap (3.37 eV) and is characterized by its high absorption and diffusion of ultraviolet radiation [6]. It is widely used in optoelectronics, catalysis, gas sensing,
photoluminescence, and piezoelectric materials [7,8]. The structural and optical properties of ZnO can be controlled and enhanced by doping, due to its partially filled 4f energy level surrounded by full 5s and 5p orbitals. Doping by the Er/Yb pair, has received much interest in the literature and has been chosen for several photonic applications [9]. The Er$^{3+}$ and Yb$^{3+}$ ions present a spectral overlap between the $2^5S_2 \rightarrow 2^5F_7/2$ band of Yb$^{3+}$ and the $4^1F_{15/2} \rightarrow 4^1I_{11/2}$ band of Er$^{3+}$, allowing the transfer of energy between these two rare earth ions, which enhances the UC process.

The synthesis routes of the doped ZnO nanoparticles are numerous, such as vapor deposition, precipitation in water solution, hydrothermal synthesis, precipitation from microemulsions, mechanochemical processes, and the sol-gel process [10]. Several studies have been conducted on the sol-gel synthesis of oxide material nanoparticles [11,12]. The sol-gel route has been considered as one of the most interesting techniques for the preparation of nanopowders, thanks to its versatility and its meticulously studied mass production potential [13]. This soft chemistry synthesis route is simple, low cost and makes it possible to have nanopowders with a size lower than 100 nm at low temperatures [14,15]. It also allows the control of the final properties of the elaborated powders [16]. Zinc acetate (Zn(CH$_3$COO)$_2 \cdot$H$_2$O), Zinc chloride (ZnCl$_2$), Zinc nitrate (Zn(NO$_3$)$_2 \cdot$6H$_2$O), and Zinc 2-ethylhexanoate (Zn(C$_8$H$_{15}$O$_2$)$_2$) are the primary precursors used in the synthesis of ZnO nanoparticles [17].

In the present work, undoped ZnO, (5 Er: ZnO), (5 Er, 5 Yb: ZnO), and (5 Er, 10 Yb: ZnO) were successfully prepared through the sol-gel process, using supercritical drying of ethyl alcohol. The Er/Yb doped ZnO nanopowders showed green and red emissions after excitation at 980 nm, via the UC mechanism. The energy band gap decreases after doping, and the electrical properties are improved. The effect of the Yb concentration on the crystallinity, UC emission, QY percentage, and electrical properties of the doped ZnO nanopowders was investigated in detail.

2. Materials and Methods

2.1. Samples Preparation

The development of the ZnO networks by the sol-gel process, took place via the inorganic polymerization reactions in the solution. These reactions were the hydrolysis at room temperature and condensation into an autoclave under high pressure until it reached the supercritical range of ethanol, in order to obtain an aerogel (Figure 1).

![Figure 1. Preparation of the (Er, Yb: ZnO) nanopowders through the sol-gel method.](image)

The solution of ZnO was prepared by dissolving a quantity of zinc acetate dihydrate (Zn(CH$_3$COO)$_2 \cdot$H$_2$O, >98%, Lobachemie), in ethanol (C$_2$H$_5$OH). For the (Er, Yb: ZnO) samples, 5% of Erbium (III) acetate hydrate (Er(CH$_3$COO)$_3 \cdot$XH$_2$O, Strem Chemicals) and (5% or 10%) of Ytterbium (III) acetate hydrate (Yb(CH$_3$COO)$_3 \cdot$XH$_2$O, Strem Chemicals) were added to the zinc precursor solution. The set was magnetically stirred at room
temperature until the total dissolution of the precursors. Then, a mixture of acetic acid (C$_2$H$_4$O$_2$) and methanol (CH$_3$OH) was added to produce H$_2$O by the esterification reaction and to ensure the hydrolysis of the solution in function of reaction (1):

$$\text{Zn(OAc)}_2 + \text{H}_2\text{O} \rightarrow (\text{OAc})-\text{Zn} + (\text{Ac})-\text{OH}$$  \hspace{1cm} (1)

Next, the obtained mixture was introduced into an autoclave. The autoclave was closed to be heated and pressurized up to the supercritical range of ethanol (T = 241 °C, P = 63 bars) [18]. During this stage, a reaction of the condensation occurred in function of reaction (2):

$$(\text{OAc})-\text{Zn}+\text{OH}-(\text{OAc}) \rightarrow (\text{OAc})-\text{Zn}-(\text{OAc}) + \text{H}_2\text{O}$$  \hspace{1cm} (2)

Following the drying cycle, a very slow expansion was performed up to the atmospheric pressure. Then, a nitrogen sweep at a low flow rate for 5 min was necessary to evacuate the rest of the solvent, remove the impurities, and reduce the mechanical stresses in the pores [19]. Finally, after 24 h, the autoclave was opened slowly to avoid cracking of the sample, due to thermal stresses and to obtain a thermal equilibrium.

The recovered undoped ZnO, (5 Er: ZnO), (5 Er, 5 Yb: ZnO), and the (5 Er, 10 Yb: ZnO) nanopowders were annealed at 500 °C. The annealing was achieved in air at a heating rate of $V = 2.5$ °C/min and a holding time of $t = 2$ h.

2.2. Measurements

The crystallinity of the nanopowders was determined by XRD, using a Bruker D8 Advance X-Ray Diffractometer, equipped with a Cu Kα ($\lambda = 1.54$ Å) source (K780 X-ray generator operating at an applied voltage of 40 kV and an intensity of 40 mA). The detection set was made of a primary Germanium monochromator and a LynxEye 1D linear detector with 192 channels covering 3° in 2. An angle interval 2θ of 20° to 85° was recorded with a pitch of 0.05° using an integration time of 20 s.

The morphology and chemical compositions of the samples were examined by SEM imaging, using SEM-FEI Quanta FEG 250 with a hot cathode field effect for the electron emission. The accelerating voltage can reach 30 kV under a high vacuum (10-4 Pa). This device was equipped with an energy dispersive X-ray spectrometer (EDS). The morphology and particle size of the nanopowders (Er, Yb: ZnO) were examined through a transmission electron microscope (TEM), and the electron diffraction was performed on a JEOL 2011 microscope operating at 200 kV with a point-to-point resolution of 0.19 nm.

The purity of the ZnO nanopowders was checked by IR-FTIR spectroscopy with a Vertex 70v vacuum FTIR spectrometer, in a spectral range of 4000–250 cm$^{-1}$ with a resolution of 4 cm$^{-1}$. The nanopowders were spread out on the surface of Si wafers.

The UC spectra of the (Er, Yb: ZnO) samples were measured using a laser diode with a 980 nm excitation source and recorded in [500–750 nm] with a Jobin–Yvin U1000 spectrometer. An Edinburgh Instruments (FLS920) spectrophotometer was used to measure the QY percentage of the nanopowders. To determine the dependence of the UC luminescence intensity upon the pumping power, the QY percentage and power density were measured by employing many filters with the same beam area for all of the measurements. The photoluminescence decays were recorded using a pulsed laser linked to a closed detection system.

The transmittance spectra were performed using a Lambda 950 spectrophotometer from Perkin Elmer in the range of 250–2500 nm.

The electrical properties were analyzed using 4-point probe resistivity measurements, using a PRO4 setup from Lucas Lab and a homemade Hall effect analyzer.

3. Results and Discussion

3.1. Structural and Morphological Studies

To study the effect of doping on the ZnO nanopowders, the XRD patterns of the undoped ZnO, (5 Er: ZnO), (5 Er, 5 Yb: ZnO), and (5 Er, 10 Yb: ZnO) aerogels, as prepared and annealed at 500 °C, are illustrated in Figure 2. All samples had a hexagonal structure.
of Wurtzite ZnO (space group P63mc, a = 3.249 Å, c = 5.205 Å, JPCDS 00-36-1451). The crystalline quality of the undoped ZnO aerogel was excellent at the prepared temperature (243 °C). In total agreement with Benammar et al. [20], no additional peak corresponding to a secondary phase or impurities was observed. This would confirm the purity of the powders developed through the sol–gel process. The appearance of new peaks assigned to the cubic structure of Erbium oxide Er$_2$O$_3$ and Ytterbium oxide Yb$_2$O$_3$, after doping the ZnO with Er/Yb was observed. We totally agree with Hu et al.’s [21] and Yaoa et al.’s [22] interpretation, stating that because the atomic rays of Er$^{3+}$ (0.89 Å) and Yb$^{3+}$ (0.86 Å) are greater than those of Zn$^{2+}$ (0.74 Å), it is difficult to incorporate all of the rare earth ions in the ZnO structures. Moreover, as was rightly reported by Chen [23] and Sangeetha, Muthukumaran and Ashokkumar [24], the formation of Er$_2$O$_3$ and Yb$_2$O$_3$ located at the grain boundaries would be caused by the coupling of the structure of the Er$^{3+}$ and Yb$^{3+}$ with the oxygen on the surface of the ZnO structure.

![Figure 2. XRD patterns of the undoped ZnO, (5 Er: ZnO), (5 Er, 5 Yb: ZnO), (5 Er, 10 Yb: ZnO) nanopowders (a) as prepared and (b) annealed at 500 °C.](image)

The Fourier transform infrared (FTIR) spectra of the undoped ZnO, (5 Er: ZnO), (5 Er, 5 Yb: ZnO), (5 Er, 10 Yb: ZnO) nanopowders, as prepared and annealed at 500 °C, are shown in Figure 3. The band between 413 and 510 cm$^{-1}$ can be attributed to the vibration of the Zn-O bond. Azam et al. [25] rightly considered this band as a characteristic band of
the hexagonal phase of Wurtzite ZnO. The FTIR spectrum of the as prepared nanopowders had bands at 1589 cm\(^{-1}\) and 2362 cm\(^{-1}\), attributed to the vibrations of the C-O bonds. Those carbonyl groups may be due to hydrocarbon contamination. The band located at 3550 cm\(^{-1}\) for the as prepared nanopowder may be attributed to the presence of alkyl groups (C-H) and would reflect an imperfection in the spectroscopic acquisition. Those bands would result from the experimental conditions that take place in the ambient air. Following the annealing at 500 °C, the bands of the carbonyl and alkyl groups disappeared, which would confirm the purity of the obtained nanopowders.

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The SEM and TEM analyses were conducted to study the morphology and size of the nanopowders. Figure 4 shows the SEM images of the effect of the Yb doping concentration on the particle morphology of the (Er, Yb: ZnO) UC nanoparticles. It can be observed that the doping obviously changed the morphology of the nanoparticles. Since ZnO has a hexagonal structure, it has a C\(_6\)v symmetry with the (0001) polar plane. This observation would confirm Zamiri et al.’s [26] finding that the (0001) basal plane has an important surface energy leading to the growth of the crystal along the C axis, which yields this
spheroidal form of ZnO nanoparticles. The morphology obtained in this study was similar to that reported by Benhebal et al. [27] for the ZnO nanoparticles developed through the sol–
gel process. The formation of a clear and highly packed grain structure was observed for
5 mol% doping of Yb, while the voids increased with an increase in the doping concentration
and the size of the grains also changed with the doping concentration.

Figure 4. SEM images of (a) the undoped ZnO; (b) (5 Er: ZnO); (c) (5 Er, 5 Yb: ZnO); (d) (5 Er,
10 Yb: ZnO) annealed at 500 °C.

Figure 5 shows the energy dispersive spectroscopy EDS (a) photos and (b) spectra of
the (5 Er, 5 Yb: ZnO) nanopowder annealed at 500 °C. Both the EDS photos and spectra of
this nanopowder confirmed the presence of Er and Yb, shown in dark blue and light blue,
respectively, in the co-doped ZnO sample.

Figure 6 illustrates the TEM images of (5 Er, 5 Yb: ZnO) annealed at 500 °C. The Figure
6a shows that the nanopowder appeared in the form of dense aggregates of crystallites.
The average size of the crystallites is about 60 nm. The hexagonal structure of the doped
ZnO nanopowder was confirmed by the selected area electron diffraction (SAED) technique
in Figure 6b. The TEM observations corroborated with the XRD and SEM analyses, in terms
of the grain structure and size measurements.
Figure 5. EDS (a) photos and (b) spectra of the (5 Er, 5 Yb: ZnO) nanopowder annealed at 500 °C.

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3.2. Up Conversion (UC) Emissions

Figure 7 shows the UC emission spectra of the (5 Er: ZnO), (5 Er, 5 Yb: ZnO) and (5 Er, 10 Yb: ZnO) nanopowders annealed at 500 °C after excitation at 980 nm at room temperature. There were two regions of visible emissions for all samples. Two emissions in the green region at 525 nm and 550 nm could be assigned to the $^4H_{11/2} \rightarrow ^4I_{15/2}$ and $^4S_{3/2} \rightarrow ^4I_{15/2}$ transitions, respectively, and an emission in the red region at 655 nm could be assigned to the red emission of the $^4F_{9/2} \rightarrow ^4I_{15/2}$ transition. When compared to other samples, the (5 Er, 5 Yb: ZnO) annealed at 500 °C, had the highest UC emission intensity and the sharpest emission peaks. These findings correlate with Lim et al.’s [28] observations of other matrices doped by Er/Yb. The UC mechanism consists of absorbing two or more photons to produce energy good enough for the UC emission. The Yb ion is a sensitizer, which absorbs the incident energy and transfers it to the Er activator ion. The activator emits radiation, producing the luminescence of the UC particles.

Figure 7. Room temperature UC emissions of the (5 Er: ZnO), (5 Er, 5 Yb: ZnO), (5 Er, 10 Yb: ZnO) nanopowder annealed at 500 °C, under 980 nm excitation.

Figure 8a illustrates the dependence of the UC luminescence intensity of (5 Er, 5 Yb: ZnO) upon the pumping power. The number of pumping photons $n$ of the (5 Er, 5 Yb: ZnO) nanopowder was calculated from the slope of the intensity UC as a
function of the laser excitation power. $n = 2.02, 2.06, 2.23$ were the values of 550 nm, 525 nm green emissions, and 655 nm red emissions, respectively. This finding would prove that the green and red emissions resulted from the two-photon UC process in this Er/Yb co-doped ZnO nanopowder.

Figure 8a illustrates the dependence of the UC luminescence intensity of (5 Er, 5 Yb: ZnO) upon the pumping power. The number of pumping photons $n$ of the (5 Er, 5 Yb: ZnO) nanopowder was calculated from the slope of the intensity UC as a function of the laser excitation power. $n = 2.02, 2.06, 2.23$ were the values of 550 nm, 525 nm green emissions, and 655 nm red emissions, respectively. This finding would prove that the green and red emissions resulted from the two-photon UC process in this Er/Yb co-doped ZnO nanopowder.

Figure 8. (a) Dependence of the UC luminescence intensity of (5 Er, 5 Yb: ZnO) upon the pumping power; and (b) energy level diagram of the Yb$^{3+}$, Er$^{3+}$ ions and the proposed UC mechanisms in (Er, Yb: ZnO) under 980 nm excitation.

To more clearly explain the results of the dependence of the UC luminescence intensity of (5 Er, 5 Yb: ZnO) upon the pumping power, the energy level diagram of the Yb$^{3+}$ and
Er$^{3+}$ ions and the proposed UC mechanisms in (Er, Yb: ZnO) under 980 nm excitation, is illustrated in Figure 8b. The UC luminescence would be the origin of the combination of multiple processes, which are the ground state absorption (GSA), energy transfer (ET), excited state absorption (ESA), and cross relaxation (CR). The UC mechanism can be presented as follows:

\[(\text{Yb}^{3+})^4F_{7/2} + \lambda_{980nm} \rightarrow ^4F_{5/2}\]

\[(\text{Er}^{3+})^4I_{15/2} + \lambda_{980nm} \rightarrow ^4I_{11/2}\]

\[(\text{Er}^{3+})^4I_{15/2} + (\text{Yb}^{3+})^4F_{5/2} \rightarrow (\text{Er}^{3+})^4I_{11/2} + (\text{Yb}^{3+})^4F_{7/2}\]

\[(\text{Er}^{3+})^4I_{11/2} + (\text{Yb}^{3+})^4F_{5/2} \rightarrow (\text{Er}^{3+})^4F_{7/2} + (\text{Yb}^{3+})^4F_{7/2}\]

Because of its short lifetime, the fast and non-radiative relaxation of the level $^4F_{7/2}$ would occur at the lower $^2H_{11/2}$ and $^4S_{3/2}$ levels. The green (525 nm and 550 nm) emissions would be, respectively, the results of the radiative transitions of $^2H_{11/2}$ and $^4S_{3/2}$ levels to the ground state level $^4I_{15/2}$, according to the following equations:

\[(\text{Er}^{3+})^2H_{11/2} \rightarrow (\text{Er}^{3+})^4I_{15/2} + \lambda_{525nm}\]

The red emission (655 nm) would be the result of a non-radiative relaxation from $^4S_{3/2}$ to $^4F_{9/2}$ level and a CR transition:

\[\text{CR: } (\text{Er}^{3+})^4F_{7/2} + (\text{Er}^{3+})^4I_{11/2} \rightarrow (\text{Er}^{3+})^4F_{9/2}\]

\[ (\text{Er}^{3+})^4F_{9/2} \rightarrow (\text{Er}^{3+})^4I_{15/2} + \lambda_{660nm}\]

The difference in intensities of the $^4S_{3/2} \rightarrow ^4I_{15/2}$ and $^2H_{11/2} \rightarrow ^4I_{15/2}$ transitions can be justified by the rapid quenching of the second transition by non-radiative relaxation. The red emission intensity is lower than the green emission because of the low cross absorption relaxation.

In order to quantify the optical response of (5 Er, 5 Yb: ZnO) annealed at 500 °C, the percentages of UC-QY and the UC emission intensities centered at 525 nm, 550 nm, and 655 nm, were measured as a function of the power density under 980 nm excitation, respectively, in Figure 9a,b. We notice that the UC-QY percentage and the emission intensities presented as follows:

Table 1 shows a summary of the results exhibited in Figure 9b. These results reflect the QY percentages of the (Er, Yb, ZnO) nanopowders annealed at 500 °C at 15.7 W/cm$^2$. The total QY percentage of (5 Er: ZnO), (5 Er, 5 Yb: ZnO), and (5 Er, 10 Yb: ZnO) was 4.59 ± 0.2%, 6.31 ± 0.2% and 3.77 ± 0.2%, respectively. As can be clearly seen in Figure 9b and Table 1, (5 Er, 5 Yb: ZnO) showed the highest values of absolute QY percentages in the green of 525 nm (1.87 ± 0.1%), in the green of 550 nm (3.37 ± 0.1%), and in the red (1.07 ± 0.2%) at 15.7 W/cm$^2$, therefore the highest value of the total QY percentage (6.31 ± 0.2%). These results are very promising, when compared to those of (3 Er, 17 Yb: β-NaYF$_4$) with 0.32% at 20 W/cm$^2$.

**Table 1.** UC-QYs measured for the (Er, Yb: ZnO) nanopowders with different concentrations of Yb at their corresponding threshold excitation power densities.

| QY Percentage at 15.7 W/cm$^2$ | Green (525 nm) (%) | Green (550 nm) (%) | Red (655 nm) (%) | Total QY Percentage |
|-------------------------------|------------------|------------------|----------------|-------------------|
| (5 Er: ZnO)                   | 1.67 ± 0.2       | 2.07 ± 0.1       | 0.85 ± 0.1     | 4.59 ± 0.2        |
| (5 Er, 5 Yb: ZnO)             | 1.87 ± 0.1       | 3.37 ± 0.1       | 1.07 ± 0.2     | 6.31 ± 0.2        |
| (5 Er, 10 Yb: ZnO)            | 1.25 ± 0.2       | 1.85 ± 0.2       | 0.65 ± 0.2     | 3.77 ± 0.2        |
These results reflect the results exhibited in Figure 9b. These results reflect the emissions centered at 525, 550 and 655 nm.

Figure 9. (a) UC intensity variations with an excitation power density for the (5 Er, 5 Yb: ZnO) nanopowder annealed at 500 °C with UC emissions centered at 525, 550 and 655 nm; (b) UC-QY percentage variation with excitation power density for the (5 Er, 5 Yb: ZnO), annealed at 500 °C with UC emissions centered at 525, 550 and 655 nm.

Figure 10a,b present the emission decay curves of (5 Er: ZnO), (5 Er, 5 Yb: ZnO) and (5 Er, 10 Yb: ZnO) at 550 nm (4S_{3/2} \rightarrow 4I_{15/2}) and 655 nm (4F_{9/2} \rightarrow 4I_{15/2}), respectively, under 980 nm excitation. As can be clearly seen, in Figure 10a, the longest excited state lifetime for the green emission had a value of 120 µs for (5 Er, 5 Yb: ZnO). Equally, Figure 10b shows that the longest excited state lifetime for the red emission, the decay time had a value of 75 µs for (5 Er, 5 Yb: ZnO). The relatively low decay time value for (5 Er, 10 Yb: ZnO) in both figures (75 µs in green and 50 µs in red), respectively, can be explained by the Er^{3+}→Yb^{3+} energy back transfer rate. 4S_{3/2} (Er^{3+}) + 2F_{7/2} (Yb^{3+}) \rightarrow 4I_{15/2} (Er^{3+}) + 2F_{5/2} (Yb^{3+}). This explanation correlates with Bergstrand et al.’s explanation of the phenomenon stating that the energy transfer depends on the distance between the Er and Yb ions as well as the dopant concentrations.
Figure 10. (a) The temporal evolution of the green (550 nm) $^4S_{3/2} \rightarrow ^4I_{15/2}$ and (b) the temporal evolution of the red (655 nm) $^4F_{9/2} \rightarrow ^4I_{15/2}$ emissions in the (Er, Yb: ZnO) nanopowders with different concentrations of Yb.

3.3. Optical Energy Band Gap

Figure 11a exhibits the transmittance spectra of the undoped ZnO, (5 Er: ZnO), (5 Er, 5 Yb: ZnO) and (5 Er, 10 Yb: ZnO), annealed at 500 °C in the range of (0–2500) nm. For all samples, the transmittance values were greater than 86% in the range of 300 to 1500 nm. Moreover, all of the doped samples exhibited a transmittance value greater than that of the undoped ZnO. Figure 11b presents the plots of the Kubelka–Munk function $(\alpha h^2)$ in function of energy $(h\nu)$, in order to calculate the energy gap of the undoped ZnO, (5 Er: ZnO), (5 Er, 5 Yb: ZnO) and (5 Er, 10 Yb: ZnO). Then, the optical energy band gap is calculated using the Tauc plot, according to the formula:

$$\alpha h \nu = A(h \nu - E_g)^n$$

where $\alpha$ is the absorption coefficient, $h \nu$ is the photon energy, $A$ is constant, $n = 1/2$ is the power factor for the direct band gap crystalline semiconductors, and $E_g$ is the energy band gap.
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The optical band gap values of ZnO, (5 Er: ZnO), (5 Er, 5 Yb: ZnO) and (5 Er, 10 Yb: ZnO) are summarized in Table 2. As can be seen, after doping, the energy band gap decreased from 3.4 eV for the undoped ZnO to 3.34 eV, 3.24 eV and 3.3 eV for (5 Er: ZnO), (5 Er, 5 Yb: ZnO), and (5 Er, 10 Yb: ZnO), respectively. This can be explained by the formation of new bands of impurities and the strong interaction between the ZnO electrons and the electrons of rare earth ions. Indeed, as was rightly explained by Munawar et al. [30] the doped rare earth ions form new intermediate energy bands in the ZnO lattice, below the conduction band, and play the role of the lowest empty molecular orbital, leading to the reduction of the band gap. In addition, the electron swapping between s-d and p-d orbitals causes a positive and a negative reorder between the valence band and the conduction band decreasing the band gap energy.
The optical band gap values of ZnO, (5 Er: ZnO), (5 Er, 5 Yb: ZnO) and (5 Er, 10 Yb: ZnO) are summarized in Table 2. As can be seen, after doping, the energy band gap decreased. In conclusion, this study attempted to design and optimize a new up-converter from the (Er, Yb: ZnO) nanopowders using the sol–gel process to enhance the efficiency and reduce the cost of solar cells. The main findings of this study were: Firstly, the nanopowder (5 Er, 5 Yb: ZnO) would have the best emission intensity in the green at 525 nm and 550 nm and in the red at 655 nm. Secondly, this up-converter would have the best QY percentage with a value of 3.24% under a power density of 15.7 W/cm². Thirdly, it had a lower band gap energy value of 3.24 eV and the best electrical properties. Fourthly, because of the availability of the materials and the relative easiness of the sol–gel process, the production of this nanopowder would have a lower cost than other materials. As a consequence, this optimized nanopowder would be recommended as a potential efficient up-converter and would be expected to enhance the cost of solar cells.

### Table 2. Optical band gap calculated from the transmittance curve, using the Tauc formula.

| Nanopowders         | Optical Band Gap (eV) |
|---------------------|-----------------------|
| Undoped ZnO         | 3.4                   |
| (5 Er: ZnO)         | 3.34                  |
| (5 Er, 5 Yb: ZnO)   | 3.24                  |
| (5 Er, 10 Yb: ZnO)  | 3.3                   |

3.4. Electrical Properties

The effect of the Yb concentration on the electrical properties of the (Er, Yb: ZnO) nanopowders was measured with the Hall effect. Figure 12 presents the resistivity (\(\rho\)), the electron mobility (\(\mu\)), and the carrier concentration (\(\eta\)) with different concentrations of Yb. As can be seen, the resistivity decreased while the electron mobility increased after doping. Hence, it can be concluded that the doped nanopowders were n-type conductors. In line with Soumahoro et al. [31], this can be interpreted as an indicator of the presence of rarest earth atoms in interstitial positions, acting as donor impurities. The carrier concentration increased until doping (5 Er, 5 Yb: ZnO) then decreased to (5 Er, 10 Yb: ZnO). In total agreement with Asikuzun et al. [32] the increase in the carrier concentration can be explained by the substitution of the Zn\(^{2+}\) ions by the rare earth ions or by the incorporation of the rare earth ions in interstitial sites, while the decrease in the carrier concentration can be explained by the increase in the grain boundary defects that trap free carriers.

![Figure 12](image-url)  
Figure 12. Resistivity (\(\rho\)), electron mobility (\(\mu\)), and carrier concentration (\(\eta\)) with different concentrations of Yb.

4. Conclusions

In conclusion, this study attempted to design and optimize a new up-converter from the (Er, Yb: ZnO) nanopowders using the sol–gel process to enhance the efficiency and reduce the cost of solar cells. The main findings of this study were: Firstly, the nanopowder (5 Er, 5 Yb: ZnO) would have the best emission intensity in the green at 525 nm and 550 nm and in the red at 655 nm. Secondly, this up-converter would have the best QY percentage with a value of 6.31 ± 0.2%, under a power density of 15.7 W/cm². Thirdly, it had a lower band gap energy value of 3.24 eV and the best electrical properties. Fourthly, because of the availability of the materials and the relative easiness of the sol–gel process, the production of this nanopowder would have a lower cost than other materials. As a consequence, this optimized nanopowder would be recommended as a potential efficient up-converter and would be expected to enhance...
the efficiency of the solar cells and allow the harvest of more solar energy at a lower cost. Finally, this UC would be suitable for many other photonic applications.

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