Theoretical and experimental investigation of the magnetic properties of polyvinylidene fluoride and magnetite nanoparticles-based nanocomposites

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Abstract

In the present study, the effect of size distribution of magnetite nanoparticles in a PVDF matrix on the magnetic properties of PVDF + Fe₃O₄ nanocomposites was experimentally and theoretically investigated. The size distribution of nanoparticles in polymer matrix and morphology of the nanocomposites were studied by the means of scanning electron microscopy and atomic force microscopy. It was found that when the Fe₃O₄ nanoparticles are introduced into the polymer matrix, their coagulation takes place. The increase in the size of the particles depends on their concentration in the polymer matrix, the type of polymer (polar, non-polar, its viscosity, etc.), reaction temperatures, etc. In addition, when Fe₃O₄ nanoparticles are introduced into the polymer network, the oxidation of the surface layer of particles occurs and the magnetic size decreases. Consequently, the reduced magnetic properties may also be observed. The hysteresis loops have been recorded in small magnetic field range. It was found that the magnetic hysteresis parameters depend on the size and concentration of Fe₃O₄ nanoparticles. Theoretical calculations were compared with experimental results obtained from \(M(H)\) measurements. The reasons of differences between theoretical and experimental results have been explained.

Keywords Magnetite · Nanocomposite · Polymer · Hysteresis · Polyvinylidene fluoride

Introduction

Magnetic nanomaterials are drawing increased attention due to their remarkable physical properties. Superparamagnetic iron oxide nanoparticles, especially magnetite phase and nanocomposites based on Fe₃O₄ nanoparticles, have attracted interest from research due to possible applications of such materials in various fields [1, 2]. The combination of different materials allows to make completely new composite materials with a wide range of functional properties: mechanical, chemical, electrical, magnetic, optical and many others [3]. Among these nanomaterials, thermoplastic polymer-based magnetic nanocomposites attract significant academic and industrial interest because of their relatively easy and low-cost producing technology.

The formation of unique properties of polymer-based magnetic nanocomposites depends on many factors such as particles size and shape, degree of dispersion, concentration.

The determination of the size of the Fe₃O₄ nanoparticles before and after their introduction into the polymer matrix has been investigated in our early works [4]. The change in nanoparticle size depends on the type of polymer.

In the presented work, the dependence of the average size of Fe₃O₄ nanoparticles in the polymer matrix on its volume content and the dependence of the magnetic properties of the composites (saturation magnetization, residual magnetization, coercive force, etc.) on the size and concentration of the filler have been investigated.
Experimental details
Materials

Polyvinylidene fluoride (PVDF) is a polar polymer that has a density of 1.78 g/cm$^3$ at 25 °C, melting point at the $T = 177$ °C.

Magnetite nanoparticles were obtained by co-precipitation method in an alkaline medium. The average nanoparticle size is 7–15 nm [1, 2].

Methods

Scanning electron microscopy (SEM)

The distribution of magnetite nanoparticles in the polymer matrix has been studied by scanning electron microscopy (SEM, JEOL JSM-7600 F). Scanning was carried out in SEI mode with an accelerating voltage of 15 kV and a working distance of 4.5 mm.

AFM analysis

The morphology of the nanocomposites was studied using atomic force microscopy Integra Prima (NT-MDT, Zele

Method for studying magnetic properties

Measurements: Magnetization curves acquired at 300 K (room temperature) by a Quantum Design SQUID magnetometer in the field range ± 50 kOe. The magnetization is reported per gram of measured sample.

Synthesis of nanocomposites

The polymer nanocomposite materials were prepared as follows: poly(vinylidene fluoride) was solved in dimethylformamide (DMF) solvent, at the room temperature. Magnetite nanoparticles were added into the polymer solution and stirred within 2 h in order to prepare a homogeneous mixture. In order to remove the solvent from the mixture, it was evaporated within 1 day.

The samples of nanocomposites were obtained by hot pressing method at melting point of PVDF under 15 MPa pressure within 4 min on further cooling to room temperature [2].

Results and discussion

Figure 1 shows SEM images of nanocomposites based on PVDF + Fe$_3$O$_4$ at various magnetite contents. As can be seen from the figure, for 1 and 3% volume contents of the filler, the sizes of magnetite nanoparticles in matrix are 13–21 nm and 29–40 nm, respectively. Using SEM images, approximately 100 particle sizes were taken for statistical parameters calculation.

The values of parameters in Gaussian and lognormal distribution of the Fe$_3$O$_4$ nanoparticles size in PVDF matrix are reported in Tables 1 and 2, respectively.

As can be seen from Table 2, the values of the standard deviation indicate a narrow lognormal particle size distribution. The values of the polydispersity index confirm the monodispersity PVDF +Fe$_3$O$_4$ nanocomposites system. This shows that the size distribution of Fe$_3$O$_4$ particles in polymer matrix is fairly good and can be described by a lognormal distribution function:

$$f(x) = \frac{1}{\sqrt{2\pi}\sigma} \cdot \exp\left(-\frac{(\ln x - \ln x_0)^2}{2\sigma^2}\right)$$

It is also clear from the table that the nature of the distribution of the Fe$_3$O$_4$ particles in the polymer matrix, as a function of their concentration and time, does not change. Only the distribution parameters ln$x$ and $\sigma$ depend on the concentration of the particles in the polymer matrix and on the time. During coagulation, the dependence of the average particle diameter on time is analogous to the dependence of the average particle diameter on the number of particles (concentration), according to the theory [5].

Figure 2 shows the lognormal distribution of Fe$_3$O$_4$ nanoparticles in PVDF matrix at different volume contents. The dependence of the average size of Fe$_3$O$_4$ nanoparticles in PVDF matrix on their concentrations was studied. Figure 3a, b represents the dependence of the average particle sizes of Fe$_3$O$_4$ nanoparticles in the polymer matrix on volume content.

As can be seen from Fig. 3a, b, the dependence curve of the Fe$_3$O$_4$ particles diameter on the concentration in PVDF matrix is complicated. At low concentrations, this dependence for PVDF matrix is weak. This is due to the particle and polymer properties. Coagulation of particles also depends on the viscosity of the polymer which it has during the preparation of the composite. In a medium with a lower viscosity, the coagulation process will happen faster. As
the concentration of the filler in the matrix increases, the viscosity of the medium changes and the coagulation condition changes as well.

The linear part of the \( d(\phi) \) dependence curve (low concentration) can be described by using the following equations:

\[
d_{\text{Fe}_3\text{O}_4} = 6.67 + 5000.0 \cdot \phi
\]  

At high concentrations of the filler, the saturation occurs, reaching at the maximum value of the coagulated particle diameter, which can be described with an exponential law (Fig. 3a).
The theory of coagulation of nanoparticles in solutions at their low concentrations is known. According to this theory, the number of particles during coagulation decreases according to the law [6, 7]

\[
\frac{dn}{dt} = -k_0 \cdot n^2
\]

The value of \( k_0 \) is defined as:

\[
k_0 = \frac{8kT}{3\eta}
\]

where \( \eta \) is the viscosity of medium.

By the definition \( \varphi_s = \frac{V_s}{V} \), where \( V_s, V \) is the volume of solid phase and medium, respectively. Since \( V_s = N \cdot V_0 \) and \( n = \frac{V}{V_0} = \frac{V_s}{V_0} \), we rewrite the last differential equation in the following form:

\[
\frac{dV}{dt} = -k_0 \varphi_s
\]

The solution is \( V_0 = k_0 \cdot \varphi_s + V_0 \). In the latter expression, if we substitute \( d_0 \), we will get the following formula:

\[
d_0 = d_0 \left( 1 + \frac{2k_0 \varphi_s}{\pi d_0^3} \right)
\]

The expression obtained is valid for low volume content of particle. As can be seen, the diameter of nanoparticles aggregated is a linear function of concentration, which is consistent with the previous results obtained (Fig. 3b). At high concentration of the filler, the last expression should be rewritten with the help of such a function that the value of the function should asymptotically approach to the fixed value “\( d \)” when the value of the variable is high.

The values of “\( k \)” were calculated with the help of (2). To determine the viscosity of the mixture, the Walter formula was used [7, 8]:

\[
\lg \gamma_m = \sum_{i=1}^{n} x_i \lg (\gamma_i + 0.6)
\]

where \( \gamma_m \) and \( \gamma_i \) are the kinematic viscosities of the mixture and the i-th component, and \( x_i \) is the fraction of the component in the medium. From the latter it is possible to determine the kinematic (further dynamic) viscosity of the mixture:

\[
\gamma_m = \exp \left( \exp \left( \sum_{i=1}^{n} x_i \lg (\gamma_i + 0.6) \right) \right)
\]

The obtained results are consistent with AFM illustrations.

Morphology of the samples and the degree of dispersion of inorganic phase in the polymer matrix were investigated using atomic force microscopy (AFM) (Fig. 4). AFM observation showed that the size of the dispersed phases increases with increasing filler content in the nanocomposites. The sizes of Fe3O4 nanoparticles are 22, 33 and 45 nm for 1, 3 and 6% volume content of filler, respectively. These results were found to be consistent with the results obtained from the theoretical calculations.

The magnetic properties of PVDF + Fe3O4-based nanocomposites were studied by experimental and theoretical investigation. Figure 6 illustrates the experimental hysteresis loops of magnetic polymer composite materials with different volume contents of the filler.

\[ M(H) \] magnetization versus magnetic field curves of PVDF + Fe3O4-based nanocomposites for different filler concentrations have a similar shape (superimposable). In this case, only the 0–50 KOe section of the \( M(H) \) curve is informative. The inset at the left panel demonstrates \( M(H) \) magnetic curve of PVDF + Fe3O4-based nanocomposites at low magnetic field. However, the whole \( m(H) \) curve of PVDF + Fe3O4 sample is coherent with a SPM behavior of this material. The inset on the left shows a small hysteresis loop close to \( H = 0 \) which is within the margin of error (Table 3).

Figure 6a, b shows the theoretical magnetization versus magnetic field curve and the magnetic susceptibility curve of a composite based on PVDF matrix and magnetite nanoparticles with size of 20 nm. Numerical differentiation was carried out by the method [9, 10].

Fig. 3 Dependence of the diameter of Fe3O4 nanoparticles on their concentration in polymer PVDF matrix. a High content of the filler; b low content of the filler.
As can be seen from Fig. 6a, b, the magnetization curves have the hysteresis loop. This is typical for particles which have many magnetic domains. The hysteresis parameters of the nanocomposites (saturation magnetization, residual magnetization, coercive force, etc.) depend on the size and concentration of Fe₃O₄ particles. As the size and concentration of Fe₃O₄ particles increase, the number of magnetic domains increases in both the particle and medium. As can be seen from Figs. 5 and 6a, the magnetic field dependence of the magnetization obtained from the experiments and calculated theoretically is close to each other for low magnetic field.

It is known that for dispersed systems, during the magnetization, the value of the saturation magnetization can be given by the following equation:

$$M_s = \varphi_m M'_s$$

where $M_s$, $M'_s$ are the saturation magnetizations of the composite and the filler, respectively, and $\varphi_m$ is the volume content of the filler.

To explain this, suppose that the geometric sizes of the nanoparticles ($d_t$) are not equal to the magnetic sizes of the nanoparticles ($d_m$).

For comparison of magnetic sizes with the geometric sizes of nanoparticles, we use the following equations:

### Table 3  Results obtained from magnetic measurements

| Sample               | $M_s$  | $M_r$  |
|----------------------|--------|--------|
| PVDF + 1 vol% Fe₃O₄ | 2.24   | 0.022  |
| PVDF + 3 vol% Fe₃O₄ | 8.01   | 0.073  |
| PVDF + 6 vol% Fe₃O₄ | 8.12   | 0.19   |

### Fig. 4  AFM image of PVDF + Fe₃O₄ nanocomposites. a PVDF + 1 vol% Fe₃O₄, b PVDF + 3 vol% Fe₃O₄ and c PVDF + 6 vol% Fe₃O₄

### Fig. 5  $M(H)$ Magnetization versus magnetic field curves of PVDF + Fe₃O₄-based nanocomposites. a (1) PVDF + 1 vol% Fe₃O₄ (2) PVDF + 3 vol% Fe₃O₄ (3) PVDF + 6 vol% Fe₃O₄. b Experimental magnetization versus magnetic field $M(H)$ curves of PVDF + Fe₃O₄-based nanocomposites under low magnetic filed for PVDF + 1% Fe₃O₄.
\[ V_t = \frac{N_t \cdot \pi}{6} d_t^3 \]

where \( \varphi_t \), \( \varphi_m \) and \( V_m \) can be given as below:

\[
\begin{align*}
\varphi_t &= V_t / V, \\
\varphi_m &= V_m / V \\
V_m &= N_m \cdot \frac{\pi}{6} d_m^3 \\
= N_m \cdot \frac{\pi}{6} (d_t - x)^3
\end{align*}
\]

where \( V, V_t \) and \( V_m \) are the volumes of medium, solid and magnetic phase, respectively. Then, by using the expression for the concentration of the magnetic phase, we obtain the relation between geometrical and magnetic phase:

\[ \varphi_t / \varphi_m = \frac{d_t^3}{(d_t + x)^3} = x \]

After the manipulation of the last expression, we get the cubic equation:

\[
\bar{x}^3 - 3 \cdot \bar{x}^2 \cdot \bar{x}^2 + 3 \cdot \bar{x} - (1 - x) \bar{d}^3 = 0 \tag{4}
\]

The last equation was solved by the Cardan method [11]. Table 4 reports the results obtained from cubic equation. It should be noted that the magnetic properties of nanocomposites are independent on the type of the polymer.

It can be concluded that the thickness of the polymer layer around nanoparticle rises with the increasing size of the nanoparticles and it also depends on the properties of the medium (molecular weight, polarity, viscosity, etc.).

It can also be seen from the table that in all cases the particle size increases, except for \( d = 20 \text{ nm} \), \( \varphi = 0.03 \), where the size decreases (i.e., the oxidation of the surface layer is close to the lattice parameter of the particle, \( a = 0.839 \text{ nm} \)).

**Conclusion**

It was found that when the Fe\(_3\)O\(_4\) particles are introduced into the polymer matrix, their coagulation takes place. The increase in the particle size depends on their concentration in the polymer matrix, the type of polymer (polar, non-polar, viscosity, etc.), reaction temperatures, etc. When Fe\(_3\)O\(_4\) particles are introduced into the polymer matrix, at the same time with the coagulation, the oxidation of their surface layer also occurs and the magnetic size decreases and hence the magnetic characteristics are reduced. It becomes clear that the magnetic hysteresis parameters depend on the size and concentration of Fe\(_3\)O\(_4\) particles in the polymer matrix. Theoretical calculations were compared with experimental results obtained from \( M(H) \) measurements. At the same time, it was shown that the magnetic field dependence of the magnetization obtained from the experiments and calculated theoretically is close to each other for low magnetic field. With increasing nanoparticle size, the difference between theoretical and experimental values increases. It is related to the fact that unlike to the reality, theoretically the magnetite nanoparticles are accepted to be single-domain.

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