Neutron scattering studies on spin fluctuations in \( \text{Sr}_2\text{RuO}_4 \)

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The magnetic excitations in \( \text{Sr}_2\text{RuO}_4 \) are studied by polarized and unpolarized neutron scattering experiments as a function of temperature. At the scattering vector of the Fermi-surface nesting with a half-integer out-of-plane component, there is no evidence for the appearance of a resonance excitation in the superconducting phase. The body of existing data indicates weakening of the scattered intensity in the nesting spectrum to occur at very low energies. The nesting signal persists up to 290 K but is strongly reduced. In contrast, a quasi-ferromagnetic contribution maintains its strength and still exhibits a finite width in momentum space.

I. INTRODUCTION

A quarter century after the discovery of superconductivity in \( \text{Sr}_2\text{RuO}_4 \) [1], its character and its pairing mechanism remain mysterious. Inspired by the ferromagnetic order appearing in the metallic sister compound \( \text{SrRuO}_3 \) [2] it was initially proposed that ferromagnetic fluctuations drive the superconductivity in \( \text{Sr}_2\text{RuO}_4 \) rendering its superconductivity similar to the A-phase of superfluid \( ^3\text{He} \) [3, 4]. For a long time chiral \( p \)-wave superconductivity with spin-triplet pairing has been considered to best describe the majority of experimental studies [5, 6] although the absence of detectable edge currents [7] and the constant Knight-shift observed for fields perpendicular to the Ru layers [8] were not easily explained in this scenario [9]. Further insight was gained from experiments performed under large uniaxial strain that revealed a considerable enhancement of the superconducting transition temperature by more than a factor two [10, 11] similar to the enhancement in the eutectic crystals [9]. However, the breaking of the four-fold axis should split the superconducting transition of the chiral state in contradiction with a single anomaly appearing in the specific heat under strain [12]. Furthermore, the strain dependence of the transition temperature close to zero strain is flat [10, 11], whereas one expects a linear dependence for the chiral state.

The picture of chiral \( p \)-wave superconductivity was fully shaken, when the two experiments yielding the strongest support for triplet pairing [13, 14] were yielding. The new studies of the Knight shift in NMR [16, 17] and those of the polarized neutron diffraction [18] reveal an unambiguous drop of the electronic susceptibility that is inconsistent with spin-triplet pairs parallel to Ru layers.

Since then, numerous proposals for the superconducting state were made mostly invoking some \( d \)-wave state and the discussion of the superconducting pairing has become very active [19–25]. The observations of broken time-reversal symmetry in muon spin relaxation experiments [26, 27] and in measurements of the magneto-optical Kerr effect [29] may require interpretations other than the chiral \( p \)-wave scenario. Many theories discuss a superconducting state with a complex combination of components [19–25].

Assuming a simple boson-mediated pairing following BCS theory, phonons and magnetic fluctuations or a combination of both [30] can be relevant. There are anomalies in the phonon dispersion that could be fingerprints of electron phonon coupling [31, 32]. The phonon mode that describes the rotation of the \( \text{RuO}_6 \) octahedra around the \( c \) axis exhibits an anomalous temperature dependence and severe broadening [31]. This mode can be associated with the structural phase transition and with the shift of the van Hove singularity in the \( \gamma \) band through the Fermi level. Both effects occur upon small Ca substitution [33, 34]. In addition, the Ru-O bond-stretching modes that exhibit an anomalous downwards dispersion in many oxides with perovskite-related structure [35] exhibit an anomalous dispersion in \( \text{Sr}_2\text{RuO}_4 \) as well [32]. Comparing the first-principles calculated [36] and measured [32] phonon dispersion in \( \text{Sr}_2\text{RuO}_4 \) the agreement is worst for these longitudinal bond-stretching modes, which exhibit a flatter dispersion indicating better screening compared to the density functional theory (DFT) calculations. Note, however, that perovskite oxides close to charge ordering exhibit a much stronger renormalization of the zone-boundary modes with breathing character that is frequently labeled overscreening [35, 37].

On the other side there is clear evidence for strong magnetic fluctuations deduced from NMR [38] and inelastic neutron scattering (INS) experiments [39, 40]. The dominating magnetic signal is incommensurate and stems from nesting in the one-dimensional bands associated
with \(d_{xz}\) and \(d_{yz}\) orbitals, see Fig. 1. The relevance of this instability towards an incommensurate spin-density wave (SDW) is underlined by the observation of static magnetic order emerging at this \(q\) position in reciprocal space for minor substitution of Ru by Ti \[46\] or of Sr by Ca \[47, 48\]. A repulsive impurity potential was recently proposed to form the nucleation center for the magnetic ordering that should strongly couple to charge currents \[49\]. Furthermore, the temperature dependence of these incommensurate magnetic fluctuations in pure \(\text{Sr}_2\text{RuO}_4\) agrees with a closeness to a quantum critical point \[10\]. These nesting-induced magnetic fluctuations can easily be explained by DFT calculations using the random phase approximations (RPA) \[50\] but their relevance for the superconducting pairing remains controversial \[51\]. Inelastic neutron scattering in the superconducting state can exclude the opening of a large gap for these nesting-driven \[52\]. Since magnetic excitations are particle hole excitations one expects in the most simple isotropic case a magnetic gap comparable to twice the superconducting one, which can be safely excluded. However, the anisotropy of the gap function and interactions can strongly modify the magnetic response in the superconducting state. A more recent TOF inelastic neutron scattering experiments confirms the absence of a large gap but reports weak evidence for suppression of spectral weight at very low energies \[53\]. This experiment also claims the occurrence of a spin resonance mode at the nesting position with a finite perpendicular wave-vector component, which would point to an essential modulation of the superconducting gap perpendicular to the \(\text{RuO}_2\) layers but which is inconsistent with the results of this work.

In addition to the incommensurate nesting-induced fluctuations, macroscopic susceptibility \[54\], NMR \[38, 55\] and also polarized inelastic neutron scattering experiments \[12, 15\] reveal the existence of magnetic fluctuations centered at the origin of the Brillouin zone, which typically can be associated with ferromagnetism. Furthermore, a small concentration Co doping can lead to static short-range ferromagnetic order \[56\]. All techniques find almost temperature independent quasi-ferromagnetic excitations in pure \(\text{Sr}_2\text{RuO}_4\). This ferromagnetic response qualitatively agrees with a recent dynamical mean field theory (DMFT) analysis of magnetic fluctuations \[57\], which finds essentially local magnetic fluctuations superposed on the well known nesting signal. However, the neutron data disagree with a fully local character as they show a finite \(q\) dependence \[55\]. The quasi-ferromagnetic fluctuations also disagree with the expectations for a nearly ferromagnetic system that exhibits paramagnon scattering \[15, 55\]. \(\text{SrRuO}_3\) clearly exhibits such paramagnon scattering with its well-defined structure in \(q\) and energy space \[55\].

Here we present additional neutron scattering experiments on the magnetic fluctuations in \(\text{Sr}_2\text{RuO}_4\), which focus on several aspects that are particularly relevant for the superconducting pairing mechanism involving magnetic fluctuations or for the general understanding of magnetic excitations in a strongly correlated electron system. We discuss the possibility of important out-of-plane dispersion in the magnetic response in the superconducting and normal states, the shape of nesting scattering away from the peak position and the non-local character of the quasi-ferromagnetic response.

II. EXPERIMENTAL

INS experiments were carried out on the ThALES \[61, 62\] and IN20 \[63\] triple-axis spectrometers (TAS) at the Institut Laue Langevin and on the LET \[64\] time-of-flight (TOF) spectrometer at the ISIS Neutron and Muon Source. We used an assembly of 12 \(\text{Sr}_2\text{RuO}_4\) crystals with a total volume of 2.2 cm\(^3\) in all experiments. At Kyoto University, the crystals were grown using the floating zone method and similar crystals were studied in many experiments \[57, 60\]. The crystal assembly was oriented in the \([100]/[010]\) scattering plane (corresponding to a vertical \(c\) axis) to study the in-plane physics of the Ru layers. Additionally, with the instruments ThALES and LET it was possible to access parts of the \(q\) space perpendicular to the plane which enables an analysis of the out-of-plane dispersion of the magnetic response. To conduct experiments inside the superconducting phase a dilution refrigerator was used, reaching a temperature of \(\sim200\) mK, well below the transition temperature of
ThALES and LET are operating with a cold neutron source providing the energy resolution to study the magnetic response down to $\sim 200 \mu$eV. The TOF spectrometer LET records data simultaneously with four different values of the incidental energies, $E_i$, and resolutions, while the energy resolution of the TAS ThALES is determined by the chosen final neutron wave vector $k_f$ of $1.57 \, \text{Å}^{-1}$ combined with the collimations. On ThALES the best intensity to background ratio was achieved by using a Si(111) monochromator and PG(002) analyzer combined with a radial collimator in front of the analyzer for further background reduction. The same configuration was also used in an earlier study [52].

A polarized neutron scattering experiment was performed on the thermal TAS IN20 using Heusler crystals as monochromator and analyzer. A spin flipper in front of the analyzer enabled the polarization analysis. The scans were performed with a fixed final momentum of $k_f = 4.1 \, \text{Å}^{-1}$, where the graphite filter in front of the analyzer cuts higher order contaminations. Longitudinal polarization analysis was performed with a set of Helmholtz coils.

III. RESULTS AND DISCUSSION

A. $q$ dependence of fluctuations associated with nesting

The TOF technique enables an imaging of the complete $Q$-$E$-space, which gives insight on the distribution of scattering intensity in the reciprocal space. Throughout the paper, the scattering vector $Q = (H, K, L)$ and the propagation vector in the first Brillouin zone $q = (q_h, q_k, q_l)$ are given in reciprocal lattice units (rlu). We mostly consider only the planar wave vector $Q_{2d} = (H, K)$ projection. Fig. 2 shows the inelastic scattering plotted against the $H, K$ components of the scattering vector in the superconducting phase. The four different panels display sections of the two-dimensional ($H, K$) plane for different incident energies and hence different resolutions. The intensities are fully integrated along the energy transfer (depending on the incident energy) and along the out-of-plane component of the scattering vector, $-0.7 < L < 0.7$. The high scattering intensities at the incommensurate positions $(\pm 0.3, 0.3)$, $(\pm 0.3, 0.7)$, and $(\pm 0.7, 0.7)$ are clearly visible, arising from the well known antiferromagnetic fluctuations [39–41, 43, 44]. Additionally there are ridges of scattering intensities connecting these positions in $[\xi, 0]$ and $[0, \xi]$ directions that were first reported in [39]. The arc visible in Fig. 2(d) connecting $(-0.3, 0.3)$ and $(0.3, 0.3)$ is a spurious signal; it does not appear for the other incident energies.

Neglecting electronic dispersion perpendicular to the planes and assuming an idealized scheme of flat one-dimensional bands originating from the $d_{xz}$ and $d_{yz}$ orbitals, one expects nesting induced magnetic excitations

![FIG. 2. In-plane scattering in the superconducting phase (T = 0.2 K). The TOF data at four different incidental energies display the magnetic scattering distribution in the $ab$ plane. The intense signal at the incommensurate positions (0.3,0.3), (0.7,0.7), and (0.3,0.7) is visible for all $E_i$. Additionally there is magnetic scattering between the incommensurate positions in $[\xi, 0]$ and $[0, \xi]$ directions, respectively. To increase the statistics the data is integrated over the maximum $L$ range of $[-0.7, 0.7]$ and full $E$ range depending on the incident energy (1.75$ < E < 10$ for $E_i = 14.13 \, \text{meV}$, 0.8$ < E < 6.7$ for $E_i = 8.78 \, \text{meV}$, 0.7$ < E < 4.5$ for $E_i = 5.64 \, \text{meV}$, and 0.5$ < E < 3.5$ for $E_i = 4.52 \, \text{meV}$). The overlayed rectangles in (a) represent the integration area of the one-dimensional cuts displayed in Fig. 3(a)-(c).]


for any two-dimensional vector $\mathbf{Q}_{2d} = (0.3, \xi)$ and $(\xi, 0.3)$ and accordingly a peak at $(0.3, 0.3)$ [50]. The peaks clearly dominate but the ridges are also detectable mostly for the positions connecting the nesting peaks, i.e. $0.3 < \xi < 0.7$. This is in accordance with the calculation of the bare susceptibility which shows an enhanced signal only between the peaks, i.e. for the paths from $(0.3, 0.3)$ to $(0.7, 0.3)$ [50].

To analyze the ridge scattering and the anisotropy of the incommensurate signals in detail, Fig. 3(a) shows one-dimensional cuts along the ridge in $[\xi, 0]$ direction calculated from the data taken with $E_i = 14.13$ meV (Fig. 2(a)). By subtracting the background obtained from the average of $(\xi, 0.15)$ and $(\xi, 0.45)$, shown in Fig. 3(b) and (c) respectively, we isolate the signal along the line $(\xi, 0.3)$ shown in Fig. 3(d). The ridge scattering is mainly detectable between the peaks at the incommensurate positions, as it is visible in the two one-dimensional cuts representing the background parallel to the ridge on both sides (Fig. 3(b) and (c)). While the $(\xi, 0.15)$ cut exhibits only a weak signal around $(-0.3, 0.15)$, the $(\xi, 0.45)$ cut shows clearly two peaks at the $(-0.7, 0.45)$ and $(-0.3, 0.45)$ positions representing the ridges in $[0, \xi]$ direction. The rounding of the one-dimensional Fermi-surface sheets suppresses the susceptibility at $(0.3, \xi)$ with $\xi$ lower than 0.3, but this suppression is not abrupt. Besides the ridge scattering we may also confirm the pronounced asymmetry of the nesting peak with a shoulder near $(0.25, 0.3)$ and equivalent positions. This shoulder was reported in [40] and was also found in the full RPA calculations.

The asymmetry of the nesting peaks and the ridge scattering between the incommensurate positions can also be seen in the data of lower incident energies (see Fig. 3(e) and (f)). The one-dimensional cuts for different $K$ values confirm the asymmetric shape of the nesting peaks. A thorough analysis of the pure magnetic signal as in the case of $E_i = 14.13$ meV is not possible due to uncertainty in the background. Furthermore, the ridge scattering is less pronounced in the data obtained with lower incident energies, which indicates a higher characteristic energy of the ridge scattering. This further explains why the much weaker scattering in the ridges has not been detected in early TAS studies [39–41].

B. Search for gap opening or a resonance mode below $T_c$

The opening of a superconductivity-induced gap in the spectrum of magnetic fluctuations would have strong impact on the discussion of the superconducting character in Sr$_2$RuO$_4$. Previous INS experiments using a TAS revealed the clear absence of a large gap at the nesting position [52], whereas a recent TOF experiment reports a tiny gap although the statistics remained very poor [53]. Studying the magnetic response of Sr$_2$RuO$_4$ in its superconducting phase by INS is challenging, because one needs to focus on small energies of the order of 0.2 to 0.5 meV. At these energies the signal in the normal state is at least one order of magnitude below its maximum strength at 6 meV, and the required high-energy resolution further suppresses statistics. Fig. 4 presents the TOF data obtained with $E_i = 3$ meV by calculating the energy dependence at the nesting position integrated over all $L$ values. The full $L$ integration is needed to enhance the statistics. In Fig. 4(a) and (b) we compare the raw data for both temperatures with the background signal. In (c) the background subtracted magnetic response in the superconducting phase is compared to that in the

FIG. 3. Magnetic scattering along the connection of the incommensurate positions. (a)-(c) show one-dimensional cuts from Fig. 2(a) along the $(\xi, K)$ paths for $K = 0.15$ (a), 0.3 (b), and 0.45 (c). The background at both sides of the incommensurate positions is displayed in (a) and (c) (represented by the same colored rectangles in 3(a)). An averaged background is formed from both (gray open circles) and fitted with a linear contribution and two Gaussians (black solid line). This is compared to the incommensurate signal in (b). In (d) the linear background contribution (black dashed line) is subtracted and the signal along the $[\xi, 0]$ direction is fitted with two skew Gaussians for the incommensurate signal and a broad Gaussian fixed at $\xi = 0.5$ (red area) taking into account the ridge scattering. (e) and (f) represent one-dimensional cuts for different $K$ and two different incident energies 8.78 meV and 5.64 meV taken from Fig. 2(b) and (c). The integration range in $[0, \xi]$ direction is ±0.025 around the $K$ value and the scans are shifted vertically for better visibility.
FIG. 4. Low energy dependence of incommensurate signal below and above the superconducting transition extracted from TOF data. (a) and (b) display the energy scans at at \(q=(0.3,0.3)\) below (\(T = 0.2\) K) and above (\(T = 2\) K) the superconducting phase transition. The background in both panels is derived from the constant \(Q\) cut at (0.09,0.41) for both temperatures (\(|Q_{IC}| = |Q_{bg}|\)). To increase statistics the TOF data with an incidental energy of 3 meV is fully integrated over \(L\) (range \([-0.7,0.7]\)) and symmetrized by folding in \(q\) space at (0.3,0.7) along the (1,-1,0) plane. The \(H\) and \(K\) component is integrated with the range \([0.25,0.35]\)

(c) Background subtraction and Bose factor correction yields the pure magnetic response at low energies which is compared inside and outside the superconducting phase.

There is no evidence for the opening of a gap within the statistics of this TOF experiment. Also a resonance at a finite energy cannot be detected. Admittedly the statistics of this TOF data is too poor to detect small signals or their suppression.

Following the claim of Iida et al. \[53\] the TOF data is also analyzed in terms of a possible resonance mode appearing at a finite value of the \(L\) component, i.e. at (0.3,0.3,0.5). Therefore, the \(L\) dependence of the magnetic signal at (0.3,0.3,\(L\)) is determined by background subtraction and compared for the two temperatures (see Fig. 5). The different panels represent the energy ranges from reference \[53\] where a resonance appearing at 0.56 meV is proposed for \(L=0.5\). In our data shown in Fig. 5(b), there is no difference visible between superconducting and normal phase at \(L=0.5\).

To study the low-energy response and its \(L\) dependence in more detail and with better statistics the TAS is better suited since measurements can be focused to single \(Q,E\) points. Using ThALES and its high flux and energy resolution constant \(Q\) scans at the incommensurate position (0.3,0.7,\(L\)) with \(L=0, 0.25,\) and 0.5 were measured to investigate the \(L\) dependence of the low energy response (see Fig. 6). This incommensurate position was chosen due to a better signal-to-noise ratio compared to (0.3,0.3,\(L\)) and because the larger \(|Q|\) value allows one to reach finite \(L\) values by tilting the cryostat. Similar to Fig. 4 (a) and (b) the raw data for two temperatures is shown in Fig. 5 (a)-(c). The background was measured by rotating \(\omega\) by 20 degrees for each \(L\) value and then combining all three backgrounds to an average. For all \(L\) values the intensity of the incommensurate signal increases approximately linearly for small energies, following the established single relaxor behavior. Comparing the two temperatures there is no difference noticable for any \(L\) value down to the energy resolution. For all \(L\) values the intensity of the incommensurate signal increases approximately linearly for small energies, following the established single relaxor behavior. Comparing the two temperatures there is no difference noticable for any \(L\) value down to the energy resolution. Especially around 0.56 meV where Iida et al. \[53\] propose a resonance at the incommensurate position...
(0.3,0.3,0.5) the two temperatures yield comparable signals. It should be noted here that while the incommensurate positions (0.3,0.3,0) and (0.7,0.3,0.5) are crystallographically not equivalent both positions become equivalent with the $L$ component 0.5, see Fig. 1. Therefore, the data taken at (0.3,0.3,0.5) and (0.7,0.3,0.5) can be compared. To emphasize the absence of a resonance mode around 0.56 meV the data from Fig. 6 is plotted with a larger energy binning to further increase the statistics (see Fig. 6 which also indicates the broad energy integration used in [53]). There is no significant deviation from the general linear behavior for any $L$ value at low temperatures detectable. Iida et al. [53] report an increase of signal of $\sim 60\%$ for $L=0.5$ in the superconducting phase, which clearly is incompatible with our data that offer higher statistics.

Since no $L$ dependence of the magnetic low energy response can be established (Fig. 6 and 7) we merge the data and compare it with the former published low-energy dependence of the incommensurate signal [52] (see Fig. 5). The new experiments below $T_c$ fully confirm that the nesting excitations in Sr$_2$RuO$_4$ do not exhibit a large gap, i.e. a magnetic gap comparable to twice the superconducting one. Combining all the previous and new data there is, however, some weak evidence for the suppression of magnetic scattering at very low energies below 0.25 meV. With the neutron instrumentation of today it seems very difficult to further characterize the suppression of the small signal at such low energy.

For the previously assumed superconducting state detailed theoretical analyzes of the magnetic response were reported [51], but concerning the more recently proposed superconducting symmetries [19–26] such investigations lack. The $d_{x^2-y^2}$ state deduced from quasiparticle interference imaging [26] exhibits nodes at Fermi-surface positions that are connected through the nesting vector. This implies that even at very low energies, the nesting induced excitations are not fully suppressed in such $d_{x^2-y^2}$ superconducting state, in agreement with the experimental absence of a large gap in the nesting spectrum [52]. Within the $d_{x^2-y^2}$ superconducting state the nesting vector also connects Fermi-surface regions with maximum and minimum gap values and it connects either two regions of the $\beta$ sheet or one $\beta$ region with an $\alpha$ region. Therefore the conditions for a spin-resonance mode are more complex and less favorable than in the case of the FeAs-based superconductors, where the $s^+$ superconducting symmetry and the nesting magnetic fluctuations perfectly match each other [65].

C. Shape of the quasi-ferromagnetic fluctuations

The polarization analysis of inelastic neutron scattering provides the separation of the magnetic from any other scattering contribution. It is therefore possible to identify a tiny magnetic response that is little structured in $q$ space. This technique was used to detect

![FIG. 6. L dependence of incommensurate signal at low energies extracted from TAS data. The constant $q$ scans were conducted at the incommensurate positions (0.3,0.7,$L$) with $L = 0, 0.25$, and 0.5 in the superconducting and normal phase. The background for each $L$ is measured after $\omega$ rotation of 20 deg, thus keeping $|q|$ constant, and later averaged for all scans, yielding the presented background (black circles) and its fit (gray). The intensity is normalized with 1980000 monitor counts which corresponds to a measuring time of about 15 min per point.](image1)

![FIG. 7. Comparison of the background-free incommensurate signal $Q=(0.3,0.7,L)$ for different $L$ values and temperatures. The compared data originates from the constant $q$ scans shown in Fig. 6. The binning is increased to $\Delta E = 0.1$ meV which yields better statistics. A linear fit (red line) provides a guide to the eye. The energy range of the proposed spin resonance [53] is indicated by the red box.](image2)
Fig. 8. Comparison of the energy dependence of the incommensurate signal with former published data from [52] (labelled: Kunkemøller PRL). Background corrected data recorded at (0.3, 0.3, 0) (circles) is given in panel (a); the background free signal at (0.3, 0.7) is averaged over all $L$ values for both temperatures (diamonds), panel (b), and the incommensurate signal reported in [52] (triangles) is shown in (c). Data were corrected for the Bose and magnetic form factors.

Quasi-ferromagnetic fluctuations and to determine their strength in comparison to the incommensurate fluctuations in Sr$_2$RuO$_4$ [45]. We wished to extend this study focusing on the $\mathbf{q}$ dependence of the magnetic quasi-ferromagnetic response. Recent DMFT calculations [57] find evidence for local fluctuations superposing the well-established nesting excitations, which qualitatively agree with the experimental quasi-ferromagnetic signal. However, while the neutron experiments indicate a finite suppression of the quasi-ferromagnetic response towards the boundaries of the Brillouin zone, the DMFT calculation obtains an essentially local feature without such $\mathbf{q}$ dependence.

The polarized neutron study was performed on the thermal TAS IN20 and the results are shown in Fig. 9. An example of the raw data with different spin channels that are needed for the polarization analysis, is given in Fig. 9(a) where a diagonal constant energy scan at 8 meV, reaching from the zone boundary (0.5, 0.5) over the incommensurate position (0.7, 0.3) to the zone center (1, 0), is shown. The $x$, $y$, $z$ indices refer to the common coordinate system used in neutron polarization analysis in respect to the scattering vector $\mathbf{Q}$ [45]. The three spin flip channels $\text{SF}_x$, $\text{SF}_y$, and $\text{SF}_z$ clearly exhibit a maximum at the incommensurate position. While $\text{SF}_y$ and $\text{SF}_z$ exhibit comparable amplitudes $\text{SF}_x$ carries the doubled intensity as it senses both magnetic components perpendicular to the scattering vector. There is an enhancement of magnetic excitations polarized along the $c$ direction, that can be seen in the stronger $\text{SF}_y$ and that was studied in reference [42]. Assuming a polarization independent background, $2I(\text{SF}_x)-I(\text{SF}_y)-I(\text{SF}_z)$ yields the background free magnetic signal, see discussion in reference [45].

Fig. 9(b) displays the magnetic signal, corrected for Bose factor, i.e. the imaginary part of the susceptibility, for different energies and temperatures. The data well agrees with the results for 8 meV and 1.6 K pre-
The quasi-ferromagnetic excitations into account, the q
processes such as electron scattering. The quasi-
tuations possess thus a larger impact on any integrat-
Around room temperature the quasi-ferromagnetic fluc-
tuations were further characterized at 290 K. The incom-
mensurate nesting signal is strongly reduced but still vis-
able, while the quasi-ferromagnetic contribution is almost
unchanged. At this temperature there is a suppression of the sig-
ral at smaller q is gradual. The TOF data confirm the
pronzed asymmetry of the nesting peaks. Concerning
the study of the nesting fluctuations at very low energy
in the superconducting phase, TAS experiments yield
higher statistics due to the possibility to focus the ex-
periment on the particular position in \( qE \) space. Data
taken at different out-of-plane components of the scatter-
ing vector exclude a sizeable resonance mode emerging at
\( L=0.5 \) in the superconducting phase. Only by combining
the results of several experiments one can obtain some
evidence for the suppression of spectral weight at very
low energies.

With neutron polarization analysis the magnetic exci-
tations were further characterized at 290 K. The incom-
mensurate nesting signal is strongly reduced but still vis-
ible, while the quasi-ferromagnetic contribution is almost
unchanged. At this temperature there is a suppression of this
quasiferromagnetic scattering at the Brillouin-zone
boundaries, which underlines that this response is not
fully local.

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IV. CONCLUSION

Polarized and unpolarized neutron scattering experi-
ments were performed to study several aspects of the
magnetic fluctuations in Sr$_2$RuO$_4$ that are particularly
relevant for a possible superconducting pairing scenario.
The TOF instrument LET yields full mapping of the
excitations and reveals the well-studied incommensurate
fluctuations at \((0,3,0.3)\) in the two-dimensional recipro-
cal space. There is also ridge scattering at \((0.3,\xi)\) re-
flecting the one-dimensional character of the \( d_{xz} \) and \( d_{yz} \)
bands, as first reported in references [43 and [44]. These
ridges are stronger between the four peaks surrounding
\((0.5,0.5)\), i.e. for \( \xi>0.3 \), but the suppression of the sig-
nal at smaller \( \xi \) is gradual. The TOF data confirm the
pronzed asymmetry of the nesting peaks. Concerning
the study of the nesting fluctuations at very low energy
in the superconducting phase, TAS experiments yield
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