RAPIDITY GAP HIGGS SIGNAL AT THE 
TEVATRON AND THE LHC†

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Abstract

We quantify the rate and the signal-to-background ratio for Higgs \( \rightarrow b\bar{b} \) detection in double-diffractive events at the Tevatron and the LHC. The signal is predicted to be very small at the Tevatron, but observable at the LHC. We show that the double-diffractive dijet production may serve as a unique gluon factory. This process can be used also as a Pomeron-Pomeron luminosity monitor.

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1 Introduction

One of the biggest challenges facing the high-energy experiments is to find a good signal with which to identify the Higgs boson. Following the closure of LEP2, the focus of searches for the Higgs is concentrated on the measurements at the present and forthcoming hadron colliders, the Tevatron and the LHC.

To ascertain whether a Higgs signal can be seen, it is crucial to show first that the background does not overwhelm the signal. For instance, as well known, an observation of the inclusive intermediate mass Higgs production, that is \( pp \) or \( p\bar{p} \to HX \) with \( H \to b\bar{b} \) is considered to be impossible because of an extremely small signal-to-background ratio due to gluon-gluon fusion, \( gg \to b\bar{b} \). One possibility which is widely discussed \[1\] is to observe the Higgs in association with massive particles (\( W/Z, t \)-quarks). Another way to reduce the background, which at first sight looks quite attractive, is to study the central production of the Higgs in events with a large rapidity gap on either side, see, for example, \[2\]–\[12\]. An obvious advantage of the rapidity gap approach is the spectacularly clean experimental signatures: hadron-free (‘no-flight’) zones between the remnants of the incoming protons and the produced system.

Let us recall \[2\]–\[4\] that, in hard production processes, a gap corresponds to a rapidity region devoid of QCD radiation and represents a footprint of the colour-singlet \( t \)-channel exchange (that is a Pomeron or \( W/Z \) or photon).

Events with large rapidity gaps may be selected either by using a calorimeter or by detecting leading protons with beam momentum fractions \( x_p \) close to 1. If the momenta of the leading protons can be measured with very high precision then a centrally produced state may be observed as a peak in the spectrum of the missing-mass (\( M \)) distribution. Indeed, it has recently been proposed \[13\] to supplement CDF with very forward detectors to measure both the proton and antiproton in Run II of the Tevatron in events with the fractional momentum loss \( \xi = 1 - x_p < 0.1 \) with extremely good accuracy, corresponding to missing-mass resolution \( \Delta M \simeq 250 \) MeV. The experimental proposal is focused on searches for the Higgs boson, on possible manifestations of the physics beyond the Standard Model, as well as on unique studies of some subtle aspects of QCD dynamics. It is expected that, in association with the high \( x_p \) protons and antiprotons, a central system with mass up to about 200 GeV can be produced at the Tevatron.

Turning to the LHC, the physics menu is extremely rich, and the studies of the central production processes, including Higgs boson searches, have some important advantages. Here we specialize on central \( H \to b\bar{b} \) production.\[5\]

In Section 2 we briefly recall the QCD mechanism for the double-diffractive production of a system of large invariant mass \( M \). We use this formalism in Section 3 to study the background for double-diffractive \( H \to b\bar{b} \) production. Then in Section 4 we present estimates for the rates of Higgs events with rapidity gaps at the Tevatron and the LHC. Finally, in Section 5, we present our conclusions.

\[1\] The discussion of \( H \to WW^*/ZZ^* \) central production as a viable way to identify the intermediate mass Higgs can be found in Refs. \[14, 15\].
2 Double-diffractive hard production processes

Here we present the estimates of the cross-sections for high energy processes of the type

\[ pp \rightarrow p + M + p, \]  

(1)

and similarly for \( p\bar{p} \), where a ‘plus’ sign indicates the presence of a large rapidity gap. To be precise, we calculate the rate for the double-diffractive exclusive production of a system of large invariant mass \( M \), say a Higgs boson. Our discussion below will be focused on the case of an intermediate mass Higgs which dominantly decays into the \( b\bar{b} \) final state.

From the outset we would like to make it clear that at present there is no consensus within the community regarding the evaluation of the double-diffractive production cross sections, see [13, 16]. The literature shows a wide range of predictions varying by many orders of magnitude. This is not so surprising, keeping in mind that the evaluation of the rate of double-diffractive hard production is in some sense analogous to an attempt to estimate the chances for two camels to go through the eye of a needle. In the latter ‘biblical’ case, the outcome crucially depends on the size of the eye, the camel’s height and on its elasticity. In order to navigate in our (back-to-earth) diffractive world it is necessary to invoke a dynamical model for the Pomeron.

![Schematic diagram of double-diffractive production of a system of invariant mass M, that is the process pp \( \rightarrow p + M + p \).](image)

Figure 1: Schematic diagram of double-diffractive production of a system of invariant mass \( M \), that is the process \( pp \rightarrow p + M + p \).

One extreme possibility is the non-perturbative approach of Refs. [5, 6] which exemplifies “soft” Pomerons (elastic camels). Another extreme [7, 8] is to consider the so-called “hard” Pomeron (inelastic camel). The “soft” Pomeron-like models give

\[ \frac{\sigma_{\text{max}}(\Pi \Pi \rightarrow H)}{\sigma_{\text{incl}}(gg \rightarrow H)} \sim \left(\frac{\sigma_{el}}{\sigma_{tot}}\right)^2, \]  

(2)

where the suppression factor containing the elastic and total \( pp \) cross sections is the probability of having two rapidity gaps, on either side of the Higgs. The low extreme, based on the “hard”
Pomeron is
\[ \frac{\sigma_{\text{min}}(\bar{P}P \rightarrow H)}{\sigma_{\text{incl}}(gg \rightarrow H)} \sim (M_H^2 \sigma_{\text{tot}})^{-2}, \]
where now the suppression factor is the probability to have a point-like dipole configuration (with the size of the eye \( \lambda \sim 1/M_H \)) in each Pomeron so that they have sufficient chance to fuse into the Higgs. These simple estimates of the suppression factor range from \( 10^{-1} \) to \( 10^{-12} \). Although naive, these results are, in fact, quite representative of the range of values that may be found in the literature.

As in Refs. [9, 10, 12, 16, 19] we adopt here the perturbative two-gluon exchange picture of the Pomeron, where the amplitude for the double-diffractive process is shown in Fig. 1. The hard subprocess \( gg \rightarrow M \) is initiated by gluon-gluon fusion and an additional relatively soft \( t \)-channel gluon is needed to screen the colour flow across the rapidity gap intervals.

A fundamental difference between the various theoretical approaches concerns the specification of the exchanged gluons. *Either* non-perturbative gluons are used in which the propagator is modified so as to reproduce the total cross section [3, 11], or a perturbative QCD estimate is made [10] using an unintegrated, skewed gluon density that is determined from the conventional gluon obtained in global parton analyses. Note that the non-perturbative normalisation based on the value of the elastic or total cross section fixes the diagonal gluon density at \( \hat{x} \sim \ell_T/\sqrt{s} \) where the transverse momentum \( \ell_T \) is small, namely \( \ell_T < 1 \text{ GeV} \) [3, 11, 20]. Thus the value of \( \hat{x} \) is even smaller than
\[ x' \approx \frac{Q_T}{\sqrt{s}} \ll x \approx \frac{M}{\sqrt{s}}, \]
where the variables are defined in Fig. 1. However, the gluon density grows as \( x \to 0 \) and so the use of a non-perturbative normalisation will lead to an overestimation of double-diffractive cross sections.

It is important to emphasize that the rapidity gap signature is very promising but, at the same time, quite a fragile tool. The gaps may easily fade away (filled by hadronic secondaries) due to various sources of QCD “radiation damage”:

(i) soft rescattering of spectator partons caused by the transverse overlap of the two incoming protons (classic minimum-bias physics);
(ii) bremsstrahlung induced by the ‘active’ partons in the hard subprocesses;
(iii) radiation originating from the small transverse distances in two-gluon Pomeron dipole.

A crucial numerical difference between the approaches concerns the size of the factor \( W \) which determines the probability for the gaps to survive in the (hostile) QCD environment\(^2\).

\(^2\)We call \( W \) the survival probability of rapidity gaps following Bjorken [4], who first introduced such a factor in the context of soft rescattering effects.
Symbolically, the survival probability \( W \) can be written as
\[
W = S^2 T^2.
\] (5)

\( S^2 \) is the probability that the gaps are not filled by secondary particles generated by soft rescattering, i.e. that no other interactions occur except the hard production process, see, for instance, [3, 4, 8, 9, 21, 22, 23, 24]. The second factor, \( T^2 \), is the price to pay for not having gluon radiation in the hard production subprocess (the so-called bremsstrahlung fee). It is related to classic Sudakov-suppression phenomena and is incorporated in the perturbative QCD calculation of the exclusive production amplitude. The soft survival factor \( S^2 \) is the “Achilles heel” of all calculations of the rates of double-diffractive processes, since \( S^2 \) strongly depends on the phenomenological models for soft diffraction. This factor is not universal, but depends on the particular hard subprocess, as well as on the distribution of partons inside the proton in impact parameter space [11, 21, 22]. It has a specific dependence on the characteristic momentum fractions carried by the active partons in the colliding hadrons [23].

In [10] we tabulated our results for the LHC using the optimistic estimate \( S^2 = 0.1 \), whereas our detailed recent calculations [22] yield a lower value, \( S^2 = 0.02 \) \((S^2 = 0.05\) for the Tevatron). However it has been pointed out [10, 24] that it is possible to check the value of \( S^2 \) by observing double-diffractive dijet production\(^3\). This process is driven by the same dynamics, and has a higher cross section, so a comparison of the measurements with the predictions can determine \( S^2 \). The recent CDF data for double-diffractive dijet production [24] appear to be consistent with our determination of \( S^2 \) in Ref. [24]. This is clear evidence in favour of the strong suppression due to the low survival probability of the rapidity gaps. Further evidence strongly supporting the adopted description of the rapidity gap physics\(^4\) comes from a good agreement (both in normalisation and shape) between the CDF measurements of the diffractive dijet distribution in the events with a leading antiproton [28] and our expectations in Refs. [23, 24]. Note that the observed relative suppression of Tevatron to HERA diffractive rates was predicted by Goulianos within the so-called renormalized Pomeron flux model [30].

The \( p^p \rightarrow p + H + (^3p^') \) cross section, corresponding to the basic mechanism shown in Fig. 1, has been calculated to single log accuracy [10]. The amplitude is
\[
\mathcal{M} = A \pi^3 \int \frac{d^2 Q_T}{Q_T^4} f_g(x_1, x'_1, Q^2_T, M_H^2/4) f_g(x_2, x'_2, Q^2_T, M_H^2/4),
\] (6)

where the \( gg \rightarrow H \) vertex factor \( A^2 \) is given by eq. (10) below, and where the unintegrated skewed gluon densities are related to the conventional distributions by
\[
f_g(x, x', Q^2_T, M_H^2/4) = R_g \frac{\partial}{\partial \ln Q_T^2} \left[ \sqrt{T(Q_T, M_H/2)} xg(x, Q^2_T) \right].
\] (7)

\(^3\)A promising idea of probing the gap survival factor in \( Z \) production by \( WW \)-fusion, with a rapidity gap on either side of the \( Z \) was advocated in Ref. 27.

\(^4\)Note that earlier CDF results [24] on diffractive \( W \) boson, dijet, \( b \)-quark and \( J/\psi \) production rates, using forward rapidity gap tagging, have already provided evidence against approaches which overlook rescattering effects.
The factor \( R_g \) is the ratio of the skewed \( x' \ll x \) integrated gluon distribution to the conventional one \([31]\). \( R_g \simeq 1.2(1.4) \) at LHC (Tevatron) energies.

The bremsstrahlung survival probability \( T^2 \) in (6) is given by

\[
T(Q_T, \mu) = \exp \left( - \int_{Q_T^2}^{\mu^2} \frac{dk_T^2}{k_T^2} \frac{\alpha_s(k_T^2)}{2\pi} \int_{0}^{1-k_T/\mu} dz \left[ z \, p_{gg}(z) + \sum_q p_{qg}(z) \right] \right). \tag{8}
\]

The origin of the factor \( 1/Q_T^4 \) in the integrand in (6) reflects the fact that the production is mediated by the ‘fusion’ of two colourless dipoles of size \( d \simeq 1/Q_T^2 \). Due to the presence of this factor it is argued (see e.g. \([11]\)) that a perturbative treatment of process (6) is inappropriate. However, it is just the Sudakov suppression factor \( T \) in the integrand, which makes the integration infrared stable and hence the perturbative predictions reliable. The saddle points of the integrand are located near \( Q_T^2 = 3.2(1.5) \) GeV\(^2\) at LHC (Tevatron) energies.

The bremsstrahlung factor \( T \) determines the probability *not* to emit the gluons in the interval \( Q_T < k_T < M_H/2 \). The upper bound of \( k_T \) is clear, and the lower bound occurs because there is destructive interference of the amplitude in which the bremsstrahlung gluon is emitted from a “hard” gluon with that in which it is emitted from the screening gluon. That is, there is no emission when \( \lambda \simeq 1/k_T \) is larger than the separation \( d \sim 1/Q_T \) of the two \( t \)-channel gluons in the transverse plane, since then they act effectively as a colour-singlet system.

In reality, both the camels and the needle’s eye, are elastic. A camel tends to be enlarged by the \( 1/(Q_T)^4 \) singularity in the integrand in (6), while the size of the eye is regulated by the QCD bremsstrahlung effects in the wavelength interval \( 1/M_H \lesssim \lambda \lesssim 1/Q_T \). The competition between these two tendencies results in the position of the saddle point of the integrand in (6), which, in turn, selects the ‘right’ camels. Regrettably, the important dampening factor \( T \) has been neglected in practically all theoretical papers on the double-diffractive Higgs or dijet production.

The amplitude (6) corresponds to the exclusive process (1). The modification for the inclusive process

\[
pp \to X + M + Y \tag{9}
\]

is given in \([8, 10, 19]\), where it was found that the event rate is much larger. However, in the inclusive case the large multiplicity of secondaries poses an additional problem in identifying the Higgs boson.

\[5\] Moreover, the effective anomalous dimension, \( \gamma \), of the gluon distribution \( xg(x, Q_T^2) \sim (Q_T^2)^{\gamma} \) additionally suppresses the contribution from the low \( Q_T^2 \) domain \([8]\).

\[6\] The only exceptions are our results in Refs. \([8, 10, 19]\) and the evaluation presented in \([11]\). However there is a clear difference in the estimate of the survival factor \( T^2 \) even between these two groups. The calculation in \([8, 10, 19]\) yields a significantly lower value of \( T^2 \) than that advocated in \([11]\).
3 Signal-to-background ratio for double-diffractive Higgs production

In order to use the ‘missing-mass’ method to search for an intermediate mass Higgs boson, via the $H \rightarrow b\bar{b}$ decay mode, we have to estimate the QCD background which arises from the production of a pair of jets with invariant mass about $M_H$, see Ref. [12] for details. Surprisingly, the critical issue of the signal-to-background ratio has never been addressed prior to Refs. [10, 12] in the, otherwise, rather vast literature on double-diffractive Higgs production. The good news is that the signal-to-background ratio does not depend on the uncertainty in the soft survival factor $S^2$, and is given just by the ratio of the corresponding $gg \rightarrow H \rightarrow b\bar{b}$ and $gg \rightarrow b\bar{b}$ subprocesses.

We begin by assuming that the $b$ jets are not tagged. Then the main background is the double-diffractive colour-singlet production of a pair of high $E_T$ gluons. This background should be compared to the double-diffractive $gg \rightarrow H$ signal, with vertex specified by

$$\frac{A^2}{4} = \frac{\sqrt{2}}{36\pi^2} G_F \alpha_S^2. \quad (10)$$

First of all, in order to reduce the background we impose a jet $E_T$-cut. For instance, if we trigger on events containing a pair of jets with angles $\theta > 60^\circ$ from the proton direction in the Higgs rest frame, then we only eliminate one half of the signal, whereas the background dijet cross section is [12]

$$\frac{d\hat{\sigma}}{dM^2} = 9.7 \frac{9\alpha_S^2}{8M^4}. \quad (11)$$

Here $M$ is the invariant mass of the dijet system.

With a common scale for the coupling $\alpha_S$, and neglecting the NLO corrections, we obtain a signal-to-background ratio

$$\frac{S}{B_{gg}} = (4.3 \times 10^{-3}) \ Br(H \rightarrow b\bar{b}) \left( \frac{M}{100 \text{ GeV}} \right)^3 \left( \frac{250 \text{ MeV}}{\Delta M} \right). \quad (12)$$

If $M_H = 120$ GeV, the ratio $S/B_{gg} \sim 5 \times 10^{-3}$. This is too small for the above approach to provide a viable signal for the detection of the Higgs boson. However the situation is greatly improved if we are able to identify $b$ and $\bar{b}$ jets. If we assume that there is only a 1% chance to misidentify a gluon jet as a $b$ jet, then tagging both the $b$ and $\bar{b}$ jets will suppress the gluon background by $10^4$. In this case only the true $b\bar{b}$ background may pose a problem.

A remarkable advantage of the double-rapidity gap signature for the $H \rightarrow bb$ events is that here the $H \rightarrow b\bar{b}$ signal/$b\bar{b}$ background ratio is strongly enhanced due to colour factors, gluon polarization selection and the spin $\frac{1}{2}$ nature of quarks [12]. First, the background $b\bar{b}$-dijet rate is suppressed due to the absence of the colour-octet $b\bar{b}$-state. Thus, for $E_T^2 < M^2/4$ we have

$$\frac{d\hat{\sigma}(gg \rightarrow b\bar{b})}{d\hat{\sigma}(gg \rightarrow gg)} < \frac{1}{4 \times 27} < 10^{-2}. \quad (13)$$
Second, we emphasize that for the exclusive process the initial $gg$ state obeys special selection rules. Besides being a colour-singlet, for forward outgoing protons, there is a strong correlation between the polarizations of two incoming gluons. Namely the fusion occurs only from the state with the projection of the total angular momentum $J_z = 0$ along the beam axis. On the other hand, the Born amplitude for light fermion pair production vanishes in this $J_z = 0$ state, see, for example, [34]. This result follows from $P$- and $T$-invariance and fermion helicity conservation of the $J_z = 0$ amplitude [35]. Thus, if we were to neglect the $b$-quark mass $m_b$, then at leading order we would have no QCD $b\bar{b}$-dijet background at all.

Of course, a non-vanishing background is expected when we allow for non-forward $b\bar{b}$ production due to the $|J_z| = 2$ admixture. However such effects appear to be very small [12]. A $b\bar{b}$ background can be also caused by the quark mass or if we emit an extra gluon. Nevertheless in the former case we still have an additional suppression to (13) of about a factor of $m_b^2/p_T^2 \simeq 4m_b^2/M_H^2 < 10^{-2}$, whereas in the latter case the extra suppression is about $\alpha_s/\pi \simeq 0.05$. Note that events containing the third (gluon) jet may be experimentally separated from Higgs decay, where the two jets are dominantly co-planar [4]. However, the price to pay for this separation is the further reduction of the signal caused by the additional Sudakov suppression of final state radiation in Higgs events [35].

Thus, the two-gluon fusion mechanism for hard production, illustrated in Fig. 1, provides a unique situation where the polarizations of the incoming two gluons are strongly correlated and only helicity zero transition occurs. An explicit calculation [12], assuming $M_H = 120$ GeV and imposing the $\theta > 60^\circ$ cut of low $E_T$ jets, gives a signal-to-background ratio

$$\frac{S}{B_{b\bar{b}}} \gtrsim 4 \left( \frac{1 \text{ GeV}}{\Delta M} \right).$$

The signal is, thus, in excess of background even at mass resolution $\Delta M \sim 2$ GeV, so the $b\bar{b}$ background should not be a problem. Unfortunately the situation worsens for inclusive Higgs production, where the polarization arguments become redundant. In this case $S/B_{b\bar{b}}$ ratio is additionally suppressed by a factor $\sim 20$–$30$.

Here I must confess that just recently the $J_z = 0$ selection rule has deceived us. When considering in Ref. [12] the double-diffractive $P$-wave heavy quarkonium production we overlooked the important point that in the non-relativistic limit the helicity-zero amplitude of the gluon-gluon coupling for the $2^{++}$ state vanishes, see, for example, [37]. Actually, such suppression was first discovered in the fifties, in the QED context for the $2^{++}$ positronium within the non-relativistic approach of Ref. [38].

After accounting for relativistic effects the $J_z = 0$ amplitude for the $2^{++} \rightarrow 2g/2\gamma$ transition

\footnote{For light quark pair exclusive production $p+p \rightarrow p+q\bar{q}+p$, with forward outgoing protons, the cancellation was first observed by Pumplin [32], see also [14, 33].}

\footnote{The situation here is similar to the signal-to-background ratio for intermediate mass Higgs production in polarised $\gamma\gamma$ collisions, which was studied in detail in [38, 39].}
no longer vanishes, although it remains relatively small \cite{9}. Therefore the results for double-diffractive exclusive tensor $\chi$-meson production given in \cite{12} are strongly overestimated.

In practice, exclusive tensor $\chi$-meson production will occur due to supposedly small corrections caused by relativistic effects in $2^{++}$ quarkonium, as well as by the off-mass-shell corrections to the $J_z = 0$ transition and by the admixture of $|J_z| = 2$ di-gluon states induced by the non-forward contributions. Unfortunately these later effects are less infrared safe than the leading pieces \cite{12} and are less perturbatively controllable. Let us recall that the helicity-zero suppression becomes redundant for inclusive quarkonium production. It is worthwhile to mention that the axial vector $(1^{++})$ heavy quarkonium double-diffractive process is strongly suppressed due to Landau-Yang theorem \cite{11}.

4 Rates for rapidity gap Higgs production

While the predictions for the $S/B_{bb}$-ratio look quite favourable for Higgs searches using the missing-mass method, the expected event rate casts a shadow on the feasibility of this approach (at least for experiments at the Tevatron). The cross section for exclusive double-diffractive Higgs production at Tevatron and LHC energies has been calculated by several authors \cite{6, 7, 9, 10, 42}. In our recent analysis \cite{22} the gap survival probability for the double-diffractive process is estimated to be $S^2 = 0.05$ at $\sqrt{s} = 2$ TeV and $S^2 = 0.02$ at $\sqrt{s} = 14$ TeV. If we incorporate these estimates into the perturbative QCD calculations \cite{10}, we find

$$\sigma_H = \sigma(pp \to p + H + \bar{p}) \simeq 0.06 \text{ fb} \quad \text{at} \quad \sqrt{s} = 2 \text{ TeV}, \quad (15)$$

$$\sigma_H = \sigma(pp \to p + H + p) \simeq 2.2 \text{ fb} \quad \text{at} \quad \sqrt{s} = 14 \text{ TeV} \quad (16)$$

for a Higgs boson of mass 120 GeV. These values correspond to the cross section ratio

$$\frac{\sigma_H}{\sigma_{\text{incl}(gg \to H)}} \simeq 10^{-4} \quad (17)$$

(c.f. eqs. (2,3)), and are much lower than the predictions of other authors listed in \cite{13}.

However, as we already mentioned, the recent CDF study of diffractive dijet production \cite{27}, provides strong experimental evidence in favour of our pessimistic estimates of the survival factor $S^2$, see \cite{24, 25}. CDF \cite{27} have studied double-diffractive dijet production for jets with $E_T > 7$ GeV. They find an upper limit for the cross section of $\sigma(\text{dijet}) < 3.7$ nb, as compared to our prediction of about 1 nb \cite{24}. Using the dijet process as a monitor thus rules out the much larger predictions for $\sigma(pp \to p + H + \bar{p})$ which exist in the literature. Unfortunately the prediction $\sigma_H \simeq 0.06$ fb of (15) means that Run II of the Tevatron, with an integrated luminosity of $\mathcal{L} = 15$ fb$^{-1}$, should yield less than an event.

\footnote{Vanishing of the forward double-diffractive $\chi(2^{++})$ production process has been recently pointed out by F. Yuan \cite{40}, who used the non-relativistic formulas for derivation of $P$-wave quarkonium production amplitudes.}

\footnote{A more complete set of references to related theoretical papers can be found in Ref. \cite{13}.}
We emphasize that such a low expected signal cross section at the Tevatron just illustrates the high price to be paid for improving the $S/B_{\bar{b}b}$ ratio by selecting events with double rapidity gaps. On the other hand, a specific prediction of the perturbative approach is that the cross section $\sigma_H$ steeply grows with energy [9, 10] (c.f. (15) with (16)), in contrast to non-perturbative phenomenological models based on Ref. [6]. In fact, if we were to ignore the rapidity gap survival probability, $S^2$, then $\sigma_H$ would have increased by more than a factor of 100 in going from $\sqrt{s} = 2$ TeV to $\sqrt{s} = 14$ TeV. However, at the larger energy, the probability to produce secondaries which populate the gaps increases, and as a result the $\sigma(pp \to p + H + p)$ increases only by a factor of 40. Nevertheless, there is a real chance to observe double-diffractive Higgs production at the LHC, since both the cross section and the luminosity are much larger than at the Tevatron. For an integrated luminosity of 100 fb$^{-1}$ at the LHC we expect, for $M_H = 120$ GeV, about 200 $H \to \bar{b}b$ events with a favourable signal-to-background ratio. Another test of our perturbative scenario is the behaviour of the dijet cross section with the jet $E_T$. Due to the $x$ dependence of the perturbative gluon, we predict a steeper fall off with increasing $E_T$ than the non-perturbative models [10].

For the inclusive production of a Higgs of mass $M_H = 120$ GeV we expect, at the LHC energy, a cross section of the order of 40(4) fb, taking rapidity gaps $\Delta \eta = 2(3)$ [10].

The double-diffractive dijet cross sections are much larger than those for Higgs production. For example, if we take a dijet bin of size $\delta E_T = 10$ GeV for each jet and $\eta_1 = \eta_2$ we obtain, for $E_T = 50$ GeV jets at LHC energies,

$$d\sigma_{excl}/d\eta|_0 \simeq 40 \text{ pb}, \quad d\sigma_{incl}/d\eta|_0 \simeq 250 \text{ pb},$$

where $\eta \equiv (\eta_1 + \eta_2)/2$. The rapidity gaps are taken to be $\Delta \eta(\text{veto}) = (\eta_{\text{min}}, \eta_{\text{max}}) = (2, 4)$ for the inclusive case (see [15] for the definition of the kinematics).

Such a high event rate and the remarkable purity of the di-gluon system, that is generated in the exclusive double-diffractive production process, provides a unique environment to make a detailed examination of high energy gluon jets. Note that in exclusive high-$E_T$ dijet events the jets appear to be pure gluon ones at the level about 3000:1. Moreover, after an appropriate selection of the two-jet configuration and the removal of the $\bar{b}b$ contamination by tagging, the sample may become (at least) an order of magnitude purer. Indeed, we may speak here of a ‘gluon factory’ [12].

Let us make the final comment on the soft suppression factor $S^2$, which has caused the main uncertainty in various calculations of the rate of rapidity gap events in the exclusive and inclusive processes of [10] and [16] respectively. This factor depends sensitively on the spatial distributions of partons inside the proton, and thus, is closely related to the whole diffractive part of the $S$-matrix, see Ref. [23] for details. For example, the survival probability for central Higgs production by $WW$ fusion, with large rapidity gaps on either side, is expected to be larger than that for the double-Pomeron exchange [11, 23]. Thus, within the approach of Ref. [23] the soft suppression factor is predicted to be $S^2 \simeq 0.25$ for the $WW \to H$ fusion at the LHC, which is about a factor of 10 above the estimate for the $PP \to H$ case.
Recall that a quantitative probe of the suppression factor $S^2$ can be achieved either by measurements of central $Z$ production [26] or of dijet production [10].

An instructive example is Higgs boson production by the $\gamma\gamma \rightarrow H$ fusion subprocess. This process takes place at very large impact parameters, where the corresponding gap survival probabilities are $S^2 = 1$ [10, 13]. $\sigma(\gamma\gamma \rightarrow H)$ is estimated to be about 0.03 fb at $\sqrt{s} = 2$ TeV and 0.3 fb at $\sqrt{s} = 14$ TeV, which is comparable to our expectations [13, 16] for double-diffractive Higgs production. Note that the strong and electromagnetic contributions have negligible interference, because they occur at quite different values of the impact parameter.

5 Conclusions

We have examined the possibility of performing a high resolution missing-mass search for the Higgs boson at the Tevatron, that is the process $p\bar{p} \rightarrow p + H + \bar{p}$ where a ‘plus’ denotes a large rapidity gap. We find that there is a huge QCD background arising from double-diffractive dijet production. A central detector to trigger on large $E_T$ jets is essential. Even so, the signal-to-background ratio is too small for a viable ‘missing-mass’ Higgs search. The situation is much improved if we identify the $b$ and $\bar{b}$ jets. The $gg \rightarrow H \rightarrow b\bar{b}$ signal is now in excess of the QCD $gg \rightarrow b\bar{b}$ background, even for a mass resolution of $\Delta M \sim 2$ GeV. The only problem is that the survival probability of the gaps takes its toll, and that as a consequence the $p\bar{p} \rightarrow p + H + \bar{p}$ event rate appears to be too small at the Tevatron. Note that remarkable agreement between the CDF diffractive dijet data [27, 28] and our predictions [23]-[25] can be viewed as a strong confirmation of the validity of our results for the gap survival probabilities. In particular, the normalization discrepancy between the CDF diffractive dijet results on $W$, dijet, $b$-quark and $J/\psi$ production [28, 29] and the expectations based on factorization, which is $O(0.1)$, clearly favours low values of $S^2$. Nevertheless, there is a real chance to observe double-diffractive Higgs production at the LHC, since both the cross section and the luminosity are much larger than at the Tevatron.

The rather pessimistic expectations of the missing-mass Higgs search at the Tevatron are, however, compensated by a by-product of the double-diffractive proposal. The double-diffractive production of dijets offers a unique gluon factory, generating huge numbers of essentially pure gluon jets from a colour-singlet state in an exceptionally clean environment [12].

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