PID Control Design for Second Order Systems

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Abstract

The Proportional Integral Derivative (PID) controllers are most commonly used in industries to compensate several numbers of practical industrial processes by the virtue of their simplicity and robustness. Several tuning methods exist for parameter tuning of PID controller. In this paper PID control design for second order system has been done with various methods. The effectiveness of tuning methods has been compared based up on time response specifications.

Index Terms: PID controller, Tuning Methods, Time-Response Specifications.

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1. Introduction

In control systems there are two types of systems, one is open loop system and another one is closed loop system. Open loop system is termed as uncontrolled system due to the absence of feedback path. Whereas closed loop system is termed as controlled system. In closed loop systems output is controlled with the help of controller and it requires one or more feedback paths and its output will be stable at desired point. PID controller is best example for closed loop systems. In 1911, Elmer Sperry developed the real PID controller. In 1922, Nicholas minor sky published the first theoretical analysis of PID controller. PID controller plays a major role in control systems engineering from the past few decades [1]. PID controller has three parameters

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likely Proportional-Integral- Derivative. The combined action of these three parameters is termed as PID controller. The working of proportional control is to optimize the steady state error by increasing the gain factor of proportional. Integral controller purpose is to eliminate the steady state error. Derivative controller main function is to decrease the overshoot and improves the system stability [2].

| Nomenclature          |
|-----------------------|
| PID Proportional Integral Derivative |
| ZN Ziegler Nichols    |
| C-H-R Chien, Hrones and Reswich |

These three individual parameters are treated as single entity in PID controller and their action improves the transient response of the system. Design of conventional PID controller are simple and easy to operate. The cost of PID controllers is low and with simple maintenance. It is widely used for industrial applications in various ways as feedback mechanism with robustness. For every application PID control systems are very unique with desired output point [6]. In previous days PID controllers have gone through analog electronics. After the invention of microprocessors, the process of all the PID controllers are done by microprocessors through digital circuits. PID controllers are also using in automation industries. Inbuilt instructions of PID controllers are in programmable logic controllers [6, 7]. PID controllers are conventionally used everywhere in the industrial applications of process control due to its reliability and flexibility.

The parameters of PID controllers are to be determined for the optimum response of the system to be controlled is referred as tuning of controller [1-4]. There are various tuning methods to found the three parameter values which gives the improvement in transient response of the system. Tuning methods are mainly classified as: (i) closed loop method (ii) open loop method. Closed loop method is nothing but operating controller in automatic state, while in open loop method in manual state. In this paper a closed loop method like Ziegler Nichols method and three open loop methods like Ziegler Nichols open loop method, C-H-R method, and Cohen Coon methods are considered to illustrate the system performance.

Yuan-Jay Wang [22] proposed a novel method to tune an optimal and robust PID controller for an open loop unstable FOPTD (First Order plus Time Delay) system. Here gain phase margin tester method and stability equation method has been used which is different from the traditional tuning methods. Against this method in [23] Yuan-Jay developed a novel alternative method which involved a graphical method to calculate all the feasible gain and phase margin specifications for robust PID controllers to stabilize a highly unstable FOPTD system. Unlike in [22] the author in [23] used both the stability equation method and parameter plane method to establish conditions of stability. Jan Cvejn in [24] developed a method to setup PI and PID controllers based on a stable FOPTD process model where dead time dynamics is manipulated without approximation. Here the main idea suggested by him was to use partial compensation which allowed using simple tuning rules which were a great advantage as the popularly used tuning rules were too complex.

The robust PID control of time delay systems usually requires the solution of complex non algebraic equations and approximating the time delay. But in [25] Wiesław Krajewski and Umberto Viora used a graphical approach to the same. Such methods simple, as they were could not be applied to more complex systems. So in [26] G. Martelli, described the stability condition based on the Pontryagins Principle. The advantage was that its complexity was directly proportional to the number of process time constants. Such results were found to be valid for lower order plants having time delay but as the order of the plant increases the complexity also rises. In paper [27] these difficulty has been dealt with. The author De-Jin Wang suggested the stabilizing range to be provided in terms of Hermite Bahler theorem. Here the time constants of the plant are assumed to be arbitrary i.e. either positive or negative. Again as in [27] De-Jin Wang used the graphical method here. The PID controller can also be used to control Nonlinear Networked Control Systems with stochastic time delays as in Haikuo He and Xin Du [28]. Here they estimated the PI controller parameters by Parzen windows and Guassian Kernels and the convergence in mean square sense has been
analysed for closed loop stochastic NCS’s. As an extension of this in [29] Xiaqian Guo and Bin Wu analysed the impact of network induced time delay on NCS and the weights of sensor controller time delay have been simulated. Furthermore the effect of plant parameters on the stability region of PID controllers was also presented.

The remaining part of the paper is organized as Section 2 describes the PID controller. In Section 3 tuning methods of PID controller have been discussed. Section 4 gives the system model and Section 5 deliberates the observation of simulation. Section 5 concludes the paper.

2. PID CONTROLLER

The basic structure of PID control system is shown in Fig.1. The difference of reference input r(t) and desired output y(t), i.e. e(t) = r(t) - y(t).

Command signal is processed for the system by controlling this error through PID controller.

\[ U(t) = K_P [e(t) + \frac{1}{T_i} \int_0^t e(t) dt + T_d \frac{de}{dt}] \]  \hspace{1cm} (1)

Therefore the following transfer function describes the PID controller in continuous S-domain

\[ G_C = P + I + D \] \hspace{1cm} (2)

\[ G_C = K_P + \frac{K_I}{s} + K_D s \] \hspace{1cm} (3)

\[ G_C = K_P \left( 1 + \frac{1}{T_I s} + T_D s \right) \] \hspace{1cm} (4)

where

\[ T_D = \text{Derivative time constant} \]
\[ T_I = \text{Integral time constant} \]
\[ K_P = \text{Proportional gain} \]
\[ K_I = \text{Integration coefficient} \]
\[ K_D = \text{Derivative time constant} \]

Fig.1. PID controller

According to Astrom and Hagglund [1], more than 95% of the control loop is of the PID type. These type of controllers are popular because of their ease in operation, robust behaviour and easy maintenance.
The effect of each parameter on the step response of the system is illustrated in Table 1.

| Parameters | Rising Time | Settling Time | Overshoot | S.S. Error |
|------------|-------------|---------------|-----------|------------|
| $k_p$      | Decreases   | Increases     | Small change | Decreases  |
| $k_i$      | Decrease    | Increase      | Increase   | Eliminate  |
| $k_d$      | Small change| Decrease      | Decrease   | Small change|

### 3. TUNING METHODS OF PID CONTROLLER

#### A. Ziegler Nichols (ZN) method of tuning

ZN methods are the most familiar method has two techniques to tune PID controller.

(i) ZN open loop method

(ii) ZN closed loop method

(i) ZN open loop technique:

This method is applied to the system along with unit step response to give the s-shaped curve as shown in Fig 2. This response of the system will be characterized by $L$ and $T$ parameters. These two parameters are reported from the tangential line to the system response of the unit step which is drawn at its inflection point \([5][8]\) and the obtained parameters are calculated according to Table 2.

| Controller | $K_p$ | $\tau_i$ | $\tau_d$ |
|------------|-------|----------|----------|
| P          | $T/L$ | $-$      | $-$      |
| PI         | 0.9$T/L$ | $L/0.3$ | $-$      |
| PID        | 1.2$T/L$ | 2$L$      | 0.5$L$   |
B. ZN Closed loop technique

In this technique, system is observed in the form of closed with controller and controller is tuned on the basis of rules given by increasing only p controller value in PID controller. i.e. nothing but increasing proportional gain value is also known as critical gain($K_{cr}$) and the time period of oscillations is referred as critical time period($P_c$)[5][8].These parameters are calculated in the below Table.3.

Table.3. PID parameter Tuning

| Controller | $K_p$ | $\tau_i$ | $\tau_d$ |
|------------|-------|----------|----------|
| P          | $0.5K_{cr}$ | -        | -        |
| PI         | $0.45K_{cr}$ | $1.2 \frac{K_{cr}}{K_p}$ | -        |
| PID        | $0.6K_{cr}$ | $\frac{2K_{cr}}{K_p}$ | $K_pP_c / 0.8$ |

C. Chien, Hrones and Reswich (C-H-R) method of tuning

Chien, Hrones and Reswich developed this method in 1952. Moderation of open loop ZN method is nothing but CHR method. This method ensures "quick response without over shoot", termed as” with 0 % overshoot” and "quick response with 20% overshoot", termed as "with 20% overshoot"[9,10]. The tuning rules of this method are given in Table 4.
Table 4. PID parameter tuning with overshoot level

| Controller | \(K_p\) | \(\tau_i\) | \(\tau_d\) | \(K_p\) | \(\tau_i\) | \(\tau_d\) |
|------------|--------|---------|---------|--------|---------|---------|
| P          | 0.3/a  | -       | -       | 0.7/a  | -       | -       |
| PI         | 0.35/a | 1.2T    | -       | 0.6/a  | T       | -       |
| PID        | 0.6/a  | T       | 0.5L    | 0.9/a  | 1.4T    | 0.47L   |

D. COHEN COON Method of Tuning

The most sensitive method compared to open loop ZN method. The tuning procedure is similar as ZN open loop and obtained parameters [9, 11] from the graph will be calculated in below mentioned in Table 5.

Table 5. PID Parameter tuning

| Controller | \(K_p\)                       | \(\tau_i\)                  | \(\tau_d\)                  |
|------------|--------------------------------|-----------------------------|-----------------------------|
| P          | \(\frac{1.03}{s^{0.34}}\)     | -                           | -                           |
| PI         | \(\frac{0.9}{s^{0.092}}\)     | \(3.33\) \(\frac{\tau + 0.092\tau_i}{\tau + 2.22\tau_i}\) | -                           |
| PID        | \(\frac{1.35}{s^{0.185}}\)    | \(2.5\) \(\frac{\tau + 0.185\tau_i}{\tau + 0.611\tau_i}\) | \(0.37\) \(\frac{\tau}{\tau + 0.185\tau_i}\) |

4. SIMULINK RESULT AND OBSERVATION

Here, second order systems is considered as

\[ G(S) = \frac{1}{s^2 + 3S + 1} \]

By using different PID tuning methods the simulation results are summarized with their time response specifications such as rise time, settling time and overshoot. The parameters of PID controller used are also shown in Table 6. and Table 7.

The unit step response of the plant using Cohen coon method is given in Fig. 3 and the performance measures are given in Table 6.
Output response of the system using CHR method based PID tuning is given in Fig.4. The response is taken for 0% overshoot. The response of the system for 20% overshoot for the same method is given in Fig.5. The response of the system with PID control design using ZN open loop method is given in Fig.6 and ZN closed loop method is given in Fig.7.

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Fig. 3. Output response of system using Cohencoon method

Fig. 4. Output response of system with CHR with 0% overshoot
Fig. 5. Output response of system with CHR with 20% overshoot.

Fig. 6. Output response of system with ZN open loop method.

Fig. 7. Output response of ZN closed loop method.
The controller parameters calculated for various types of control design are tabulated in Table 6. The performance of the system for various types of control design using time response specifications are tabulated in Table 7.

Table 6. Controller parameters for System with various methods

| METHOD                          | $K_P$ | $K_I$ | $K_D$ |
|---------------------------------|-------|-------|-------|
| Z-N METHOD (OPEN LOOP)          | 18    | 0.6   | 0.15  |
| Z-N METHOD FOR (CLOSED LOOP)    | 417   | 1250  | 125   |
| COHEN COON                      | 189.18| 0.0498| 0.00739|
| C-H-R(0% OVERSHOOT)             | 6     | 4.6   | 0.15  |
| C-H-R(20% OVERSHOOT)            | 9     | 6.44  | 0.141 |

Table 7. Comparison of various transient parameters

| METHOD                          | OVERSHOOT | RISE TIME | PEAK RESPONSE | SETTLING TIME |
|---------------------------------|-----------|-----------|---------------|---------------|
| Z-N METHOD (OPEN LOOP)          | 23.8%     | 0.339 SEC | 1.24          | 27.7 SEC      |
| Z-N METHOD FOR (CLOSED LOOP)    | 21.9%     | 0.0134 SEC| 1.22          | 0.0718 SEC    |
| C-H-R(0% OVERSHOOT)             | 26.5%     | 0.635 SEC | 1.27          | 3.42 SEC      |
| C-H-R(20% OVERSHOOT)            | 31.1%     | 0.481 SEC | 1.31          | 3.74 SEC      |
| COHEN COON                      | 69.9%     | 0.0826 SEC| 1.7           | 0.0718 SEC    |

From the results of various transient performance specifications, it can be observed that there is significant amount of improvement in results with ZN method of closed loop approach for some measures. Specifically, from the transient performance indices point of view, the ZN method of closed loop approach results in better performance in terms of settling time and CHR method of tuning gives better performance in terms of rise time. The ZN closed loop method gives superior results in terms of overshoot and settling time.

5. CONCLUSION

The majority of the modern control systems in industries are being controlled by the Proportional-Integral-Derivative (PID) controller. There are many methods available to set the parameters of the PID controllers. But the stability analysis of the systems using PID controllers still remain difficult and there are only a few existing results on the PID controller synthesis. The main aim is to tune the PID parameters of the controller. Paper describes PID controller design for a second order system. Tuning techniques were enforced and their performance is examined by considering a second order system. The performance of PID control design for the considered second order system has been evaluated with the help of time response specifications. From the results, it has been observed that the system exhibits large overshoot with Cohen-Coon tuning technique and largest settling time with Ziegler Nicholas open loop method. Ziegler
Nicholas closed loop tuned PID exhibits less overshoot and settling time. Among all PID tuning techniques considered, it has been concluded that the Ziegler Nicholas closed loop tuned PID controller gives the best results for the second order system. The PID controller has some limitations such as, it works best for the processes that are linear and time invariant. This controller gives unsatisfactory results for the systems with nonlinearities, time variant and having uncertainties. In real applications, the proper tuning of the controller gains is still an open problem with this control. However, the future scope of this work includes tuning of PID controller for the systems with time delay.

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