SOLAR-CYCLE VARIATION OF SOUND SPEED NEAR THE SOLAR SURFACE

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ABSTRACT

We present evidence that the sound-speed variation with solar activity has a two-layer configuration, similar to the one observed below an active region, which consists of a negative layer near the solar surface and a positive one in the layer immediately below the first one. Frequency differences between the activity minimum and maximum of solar cycle 23, obtained applying global helioseismology to the Michelson Doppler Imager on board the Solar and Heliospheric Observatory, is used to determine the sound-speed variation from below the base of the convection zone to a few Mm below the solar surface. We find that the sound speed at solar maximum is smaller than at solar minimum at the limit of our determination (5.5 Mm). The min-to-max difference decreases in absolute values until \( \sim 7 \) Mm. At larger depths, the sound speed at solar maximum is larger than at solar minimum and the difference increases with depth until \( \sim 10 \) Mm. At this depth, the relative difference \( \frac{\delta c^2}{c^2} \) is less than half of the value observed at the lowest depth determination. At deeper layers, it slowly decreases with depth until there is no difference between maximum and minimum activity.

Key words: methods: data analysis – Sun: activity – Sun: helioseismology – Sun: interior – Sun: oscillations

Online-only material: color figures

1. INTRODUCTION

The Sun has an approximately 22 year magnetic cycle, where the dipolar magnetic field at the solar poles reverses each 11 years or so. During the reversal, the magnetic activity is at a minimum and very few sunspots are visible on the Sun; sometimes none can be seen. At the maximum in the cycle, the number of sunspots visible on the Sun can be more than 100 at one time. A typical sunspot has a lifetime of a few weeks. The radio, ultraviolet, and X-ray emission of the Sun also increase significantly during solar maximum. The total solar irradiance too has a strong correlation with the sunspot number. Significant flares occur at all phases of the sunspot cycle, but the number of M-class and X-class flares tends to follow the sunspot number. There are several proxies of solar activity currently used, probing M-class and X-class flares tends to follow the sunspot number. Significant flares occur at all phases of the sunspot cycle, but the number of M-class and X-class flares tends to follow the sunspot number. There are several proxies of solar activity currently used, probing M-class and X-class flares tends to follow the sunspot number.

As initially reported by Woodard & Noyes (1985), it is now well established that the frequency of the solar acoustic modes is strongly correlated with solar activity. This has been observed for modes with a degree up to 3 (e.g., Salabert et al. 2004; Chaplin et al. 2007), up to about 200 (e.g., Bachmann & Brown 1993; Jain & Bhatnagar 2003; Antia 2003; Dziembowski & Goode 2005; Jain et al. 2009), and up to 1000 (e.g., Rhodes et al. 2002, 2011; Rabello-Soares et al. 2006; Rabello-Soares 2011). The observed mode frequencies can be inverted to obtain the sound speed in the solar interior where the waves travel through. However, in analyzing the changes in mode frequency with the magnetic solar cycle, we have to keep in mind that magnetic fields can change not only the thermodynamic structure of the medium the waves travel through, which, in turn, changes the frequencies of the waves but also the plasma waves can be directly affected by the magnetic fields through the Lorentz force. In short, the modification to the acoustic mode frequencies results from both structural and non-structural effects of the magnetic fields (see Lin et al. 2006).

The measured solar-cycle frequency shifts depend strongly only on the frequency of the mode after they have been weighted by the mode inertia (Libbrecht & Woodard 1990). This indicates that the dominant structural changes during the solar cycle, so far as they affect the mode frequencies, occur near the surface. At the outermost layers, the timescale of the heat transfer is smaller than the period of the oscillation and they are not adiabatic anymore. At the moment, there is no general agreement as to the precise physical mechanism near the surface that gives rise to the frequency variation (see, for example, Li et al. 2003). Several authors confirmed that all or most of the physical changes were confined to the shallow layers of the Sun (e.g., Basu 2002; Eff-Darwich et al. 2002; Dziembowski & Goode 2005; Rabello-Soares & Korzennik 2009, etc). However, Baldner & Basu (2008) observed a small but significant change in the sound speed at the base of the convective zone and for \( r \gtrsim 0.9 R_\odot \). A change in the interior structure was also found by Basu & Mandel (2004), specifically a variation in the adiabatic index, \( \Gamma_1 \), near the second helium ionization zone (\( \sim 0.98 R_\odot \)). On the other hand, changes in zonal and meridional flows correlated with solar activity have been observed by several authors (Schou 1999; Howe et al. 2000; Vorontsov et al. 2002; Howe et al. 2005; Basu & Antia 2006, etc).

Local helioseismology techniques have shown that below an active region there is a two-layer structure with a negative variation of the sound speed in a shallow subsurface layer and a positive variation in the deeper interior relative to a quiet-Sun region (see Kosovichev et al. 2000; Basu et al. 2004; Bogart et al. 2008; Kosovichev et al. 2011, and references within). A similar variation has been observed for the adiabatic index, \( \Gamma_1 \), below an active region (Basu et al. 2004; Bogart et al. 2008). Because global activity levels are much smaller than in active regions, a similar structure variation would be much smaller on a global scale, if it occurs at all.

Rabello-Soares (2011) estimated the frequency differences between the activity minimum and maximum by carefully fitting the variation of the acoustic mode frequency with solar activity for modes with \( 20 \lesssim l \lesssim 900 \) observed by the Michelson
Two different peak-fitting algorithms were used to fit the power spectra and obtain the mode frequencies. One of them, known as the MDI peak-fitting method, is described in detail by Schou (1992; see also Schou et al. 2002; Larson & Schou 2008, 2009). A spherical-harmonic decomposition is not orthonormal over the solar surface that can be observed from a single viewpoint resulting in what is referred to as spatial leakage. At high degrees, the spatial leaks lie closer in frequency (due to a smaller mode separation), resulting in the overlap of the target mode with the spatial leaks that merge individual peaks into ridges, making it more difficult to estimate unbiased mode frequencies. The MDI peak-fitting method works very well for low- and medium-$l$ modes where the leaks are well separated from the target mode. For high-$l$ modes, which have spatial leaks overlapping the target mode and blended in a single ridge, the Korzennik (1998) method was used (for details, see Rabello-Soares et al. 2008). The fitting was carried out only for every tenth $l$ for modes with $100 \leq l \leq 900$. This method was applied only to the Dynamics time series which were Fourier-transformed in small segments (4096 minutes) whose spectra were averaged to produce an averaged power spectrum with a low but adequate frequency resolution to fit the ridge while reducing the realization noise. These two peak-fitting methods will be called ML and HL, respectively.

The ML method was applied to both observing sets and the HL only to the Dynamics set. In summary, three types of data were used in this work: (1) frequencies obtained by both ML and HL methods applied to the Dynamics set (“Dynamics ML+HL”), (2) frequencies obtained by only the ML method applied to the Dynamics set (“Dynamics ML”), and (3) frequencies obtained by only the ML method applied to the Structure set (“Structure ML”).

The estimated mode frequencies, $\nu_{nlm}$, were parameterized in terms of Clebsch–Gordan coefficients (Ritzwoller & Lavely 1991). The central frequency, i.e., the frequency free of splitting effects, is taken to be the frequency given by $m = 0$ in the parameterization. For each of these three sets, the central frequency, $\nu_C$, for each time period was fitted assuming a linear and a quadratic relationship with the correspondent solar-activity index and using a weighted least-squares minimization. For a detailed description, see Rabello-Soares (2011). The solar radio 10.7 cm daily flux (NGDC/NOAA) was used as the solar-activity proxy (Figure 1).

Although there is a very high linear correlation of the mode frequency variation with several solar-activity indices, deviations from a simple linear relation have been reported (see, for example, Chaplin et al. 2007). More recently, Rabello-Soares (2011) found some evidence of a quadratic relationship indicating a saturation at high solar activity ($\sim 350 \times 10^{-22} \text{ J s}^{-1} \text{ m}^{-2} \text{ Hz}^{-1}$). A similar effect has been seen in frequencies at activity regions with a large surface magnetic field using ring analysis (Basu et al. 2004). The frequency shifts obtained using the quadratic fitting were used here.

Modes with a negative linear coefficient in the quadratic fitting were excluded from the present analysis. They also have a positive quadratic coefficient, indicating that they are less affected by low and medium levels of solar activity. They correspond to 5%, 11%, and 16% of the modes of the Structure ML, Dynamics ML, and Dynamics ML+HL sets, respectively. In the Dynamics ML+HL mode set, the excluded modes make for the lack of modes in the middle of the $l - \nu$ diagram in Figure 2. The $f$-modes obtained with the HL method (about 20 modes) have a distinctive behavior from those obtained with the ML method (see Figure 7 in Rabello-Soares 2011). It is not clear if this behavior is an artifact of the frequency determination or not. They were excluded from our analysis.

The solar-activity minimum-to-maximum frequency shift $\delta \nu_{\text{ML}}^l$ is defined as the difference between the fitted frequency at the maximum and at the minimum of solar activity. The minimum and maximum activity correspond to the Dynamics observing periods centered around 2008 April and 2002 May, respectively.
Figure 3. Scaled minimum to maximum frequency differences obtained using Dynamics ML+HL (black squares), Dynamics ML (black crosses), and Structure ML (small black circles) sets. Green, red, and blue circles (gray, dark gray, and light gray in the printed journal) correspond to the averaged values for Dynamics ML+HL, Dynamics ML, and Structure ML, respectively. The solid lines are the interpolated splines representing the surface term, $F_{\text{surf}}$. (A color version of this figure is available in the online journal.)

Figure 4. Residuals, $Q_{nl} \delta \nu_{nl}/\nu_{nl}$, obtained after subtracting $F_{\text{surf}}$. The black squares, red crosses (gray in the printed journal), and blue circles (light gray in the printed journal) correspond to Dynamics ML+HL, Dynamics ML, and Structure ML, respectively. (A color version of this figure is available in the online journal.)

Figure 5. Relative frequency differences between solar maximum and minimum, after removing the surface term, used in the sound-speed inversion. (A color version of this figure is available in the online journal.)

3. THE SURFACE TERM

The scaled frequency differences $Q_{nl} \delta \nu_{nl}/\nu_{nl}$ (between two models or between the Sun and a model) can be expressed as $H_1(\nu_{nl}/L) + H_2(\nu_{nl})$, where $H_1$ is the contribution of the interior sound-speed difference, $H_2$ of the differences in the surface layers, $Q_{nl}$ is the mode inertia normalized by the inertia of a radial mode of the same frequency, and $L = \sqrt{l(l+1)}$ (Christensen-Dalsgaard et al. 1989). $H_2$ is also called the surface term, $F_{\text{surf}}$.

Figure 3 shows the scaled frequency differences between solar minimum and maximum, $Q_{nl} \delta \nu_{nl}/\nu_{nl}$, obtained using the Dynamics ML+HL (black squares), Dynamics ML (black crosses), and Structure ML (small black circles) sets. They are basically a function of frequency. The near-surface contribution can be removed by subtracting a smooth function of frequency, $F_{\text{surf}}(\nu)$, from the scaled frequency shifts, thus allowing the search for structure variations in the solar interior with the solar cycle. $Q_{nl} \delta \nu_{nl}/\nu_{nl}$ were averaged over 200 $\mu$Hz intervals. In each interval, outliers large than 3 $\sigma$ were removed and the weighted average calculated. The results are represented in Figure 3 as green, red, and blue circles (gray, dark gray, and light gray in the printed journal), respectively, for the Dynamics ML+HL, Dynamics ML, and Structure ML sets. A cubic spline interpolation was applied to the 17 and 21 frequency-knots for the ML and ML+HL sets, respectively (solid lines in Figure 3). Figure 4 shows the residuals after subtracting the surface term given by the splines.

4. RESULTS

A nonasymptotic inversion technique can be applied to infer the sound speed (and density) inside the Sun using the frequency differences between the Sun and a reference solar model (e.g., Antia & Basu 1994, and references within). Here the solar-cycle frequency shifts, $\delta \nu_{nl}$, were inverted to determine the differences in sound speed between minimum and maximum solar activity inside the Sun. The inversion has been carried out using the multiplicative optimally localized averages technique (Gough 1985). The relative frequency shifts $\delta \nu_{nl}/\nu_{nl}$ are plotted in Figure 5. They are small, indicating small changes in the solar structure with the solar cycle, if any.

The inferred sound-speed differences are shown in Figure 6. The results obtained using the Dynamics ML+HL (black), Dynamics ML (red; gray in the printed journal), and Structure ML (blue; light gray in the printed journal) sets follow the same general trend. The sound-speed difference increases slowly with radius until about 0.98 $R_\odot$ after which it decreases sharply. The sound-speed difference is larger than 6 $\sigma$ at its maximum for all three sets. The inversion results are identical if a linear fit of the mode frequencies to the solar-activity index is used instead of a second-degree polynomial.

The solution errors for the Dynamics ML+HL set are smaller by as much as 25% compared with the other two sets for $r >$
Figure 6. Inferred sound-speed differences obtained using Dynamics ML+HL (black circles), Dynamics ML (red line; gray in the printed journal), and Structure ML (blue line; light gray in the printed journal) sets. The bottom panel shows the solution near the surface in more detail. The vertical dotted lines mark approximately the regions that correspond to positive, zero, and negative sound-speed variations below an active region in relation to a quiet region obtained by ring analysis (Bogart et al. 2008).

(A color version of this figure is available in the online journal.)

Figure 7. Top: samples of averaging kernels at five different radii near the surface for the Dynamics ML+HL set. The target radius is shown by a vertical dotted line. Bottom: averaging kernels at $r = 0.992 R_\odot$ for Dynamics ML+HL (solid line), Dynamics ML (dashed line), and Structure ML (dotted line) sets. The cross-term kernel is also plotted for all three sets. It is multiplied by 100 and displaced vertically by $-30$ for visualization purpose.

Figure 8 shows the sound-speed difference between two different solar models (solid red line; gray in the printed journal) and the correspondent inversion results (black circles) obtained using the same mode set as our observations given by Dynamics ML+HL. The inversion results are very similar using any of the other two sets. The two solar models are Model S and a model with identical physical assumptions but with a lower solar age, 4.52 Gyr, instead of 4.6 Gyr (Christensen-Dalsgaard et al. 1996). The inversion results agree very well with the true model difference for $r \leq 0.992 R_\odot$, especially taking into account the averaging kernel (dashed red line in the bottom panel; gray in the printed journal).

Howe & Thompson (1996) showed that random noise in the observed mode frequency will introduce spurious oscillatory structures in the solution as a result of the correlation of the errors in the solution at different radii. The inversion result at two different radii makes use of similar data sets and their correspondent errors. The solution errors are correlated even between points farther apart than the averaging kernel width. For examples of sound-speed error correlation, see Rabello-Soares et al. (1999) and Basu et al. (2003). To illustrate the effect of the error correlation in the inversion results presented here, it was carried out inversions of the theoretical frequency differences between the two models with noise added to them. To each frequency difference the noise was generated as normally distributed random numbers with the same standard deviation as the error in the observed data. The solid black line in Figure 8 shows the result for one realization. The spurious oscillatory structures introduced by the correlated errors, also present in Figure 6, are clearly seen. The two dotted lines correspond to the average of 1000 realizations plus and minus $2.5\sigma$, showing that the overall results are consistent with the estimated formal errors.

0.85 $R_\odot$ and 15% for $r < 0.85 R_\odot$. Also, the averaging kernels for Dynamics ML+HL are slightly more localized close to the surface compared with the other two sets due to the inclusion of high-$l$ modes. In Figure 6, the averaging kernel widths (defined as the difference between the first and third quartile points) are given by the horizontal error bars for a few selected locations. In the top panel, the horizontal bars are the same for all three sets. In the bottom panel, they are in black for Dynamics ML+HL and in red (gray in the printed journal) for the Dynamics ML and Structure ML sets, since they are very similar. Nevertheless, the averaging kernels are well localized and have almost no side lobes for the inferred solution from 0.53 to 0.992 $R_\odot$ for all three sets (Figure 7). The cross-term kernel measures the influence of the contribution from density on the inferred sound speed and it is insignificant in this range (bottom panel). We did not include modes with $l < 20$ in our analysis since we are not interested in the solar deeper layers here. For $r > 0.992 R_\odot$, the averaging kernels become increasingly asymmetric and develop large side lobes.

To check that the surface term is properly removed and is not causing the observed sound-speed variation, the surface term was estimated using four times more frequency-knots than used in Figure 3 (i.e., using 50 $\mu$Hz intervals). In this case, $F_{\text{surf}}$ is not a smooth function of frequency anymore. The inversion of the residuals is still similar to Figure 6. The maximum sound-speed variation around 0.98 $R_\odot$ is still statistically significant; it is larger than $4\sigma$ (larger than $6\sigma$ for the Dynamics ML+HL set).
Figure 8. Sound-speed differences between two solar models through most of the solar interior (top) and, in detail, near the surface (bottom). The solid red line (gray in the printed journal) is the true difference between the models, while the dashed gray line (bottom panel) is the difference weighted by the averaging kernels. The black circles represent the inversion results using the observed mode set for Dynamics ML+HL and the solid black line the inversion results with random noise added to the theoretical frequencies. The two dotted black lines correspond to the average of 1000 realizations plus and minus 2.5σ.

(A color version of this figure is available in the online journal.)

Figure 9. Black circles and diamonds are the inversion results using Dynamics ML+HL and Dynamics ML, respectively. They are identical to the black and red (gray in the printed journal) circles in Figure 6. The red (gray) line is the smooth function, \( \tilde{\delta}c^2/c^2 \), which was weighted by the averaging kernels and fitted to the inversion results of the two Dynamics sets. The blue (light gray) line is \( \tilde{\delta}c^2/c^2 \) weighted by the averaging kernels.

(A color version of this figure is available in the online journal.)

To remove the spurious oscillation in our sound-speed determination, a sum of two Gaussian functions was arbitrarily chosen as a smooth function of radius, \( \tilde{\delta}c^2/c^2(r) \). It was “weighted” by the averaging kernels and fitted to the inversion results of the two Dynamics sets using a nonlinear least-square fit (red solid line in Figure 9; gray in the printed journal). According to this simple model, the sound-speed difference increases with radius from around the base of the convection zone until 0.985\( R_\odot \) (i.e., 10 Mm below the surface) at the second helium ionization zone where \( \tilde{\delta}c^2/c^2 = 3.9 \times 10^{-4} \). Closer to the surface, it decreases steeply with radius. It is zero at 0.990\( R_\odot \) (i.e., at a depth of 7 Mm) and, at 0.992\( R_\odot \) (or 5.5 Mm deep), \( \tilde{\delta}c^2/c^2 = -9.2 \times 10^{-4} \), where the sound speed at solar maximum is smaller than at solar minimum.

5. DISCUSSION

Using global helioseismology, Baldner & Basu (2008) found an increase with radius in the sound-speed variation with solar cycle for 0.86 < \( r/R_\odot \) < 0.95 (at the equator and at 15° in latitude) that agrees with our results within less than 1.5σ. Here, we found that the variation in sound speed increases until 0.985\( R_\odot \) after which it decreases fast with radius, becoming negative for \( r > 0.990 R_\odot \). This raises the question of what the physical mechanism behind this sudden change in behavior is at this particular depth.

This crossing of the sound speed at solar maximum from larger to smaller than at solar minimum is consistent in location with the crossing of the sound speed below an active region from larger to smaller than at a quiet region obtained by ring-diagram analysis (Basu et al. 2004; Bogart et al. 2008). The vertical lines in Figures 6 and 9 mark approximately the regions that correspond to Figure 9 in Bogart et al. (2008) for positive, zero, and negative sound-speed variations below an active region in relation to a quiet region. This agreement indicates that the sound-speed variation in the solar interior with solar cycle might be an overall effect of the active region’s local perturbation, and not a global structure change with solar activity. The estimated sound-speed variation obtained here is based on averages over the whole Sun at a particular depth and over one or more solar rotations.

The number of active regions is very well correlated with the solar-activity cycle. Using the data provided by SIDC (Solar Influences Data Analysis Center of the Royal Observatory of Belgium), the daily sunspot number averaged over the maximum-activity observing period (centered around 2002 May) is about 120, while during the minimum (2008 April) it is less than 10. According to ring-diagram analysis, the sound-speed variation at a depth of 14 Mm (i.e., 0.98\( R_\odot \)) below a 16° × 16° region on the solar surface (tracked for 5.7 days) with a strong active region and with a magnetic activity index (MAI) of about 80 G in comparison to a quiet region is \( \delta c^2/c^2 \approx 0.01 \) (Basu et al. 2004). For a smaller sunspot with an MAI of 40 G, it is 0.05. In brief, the MAI is the average of MDI magnetograms over the same area in the solar surface and the same observing time as the analyzed region (for a full definition, see Basu et al.)
be estimated the sound-speed difference between solar maximum by MDI above the detected signal.

Time distance is another local helioseismology technique that provides information about the subsurface structure of active regions. While the ring-diagram technique is based on the analysis of three-dimensional power spectra in a small region of the Sun to measure the oscillation frequencies (Hill 1988), as in global helioseismology, time distance measures the wave travel times between different points on the surface (Duvall et al. 1997). Both the ring-diagram and time-distance techniques give qualitatively similar results, revealing a characteristic two-layer seismic sound-speed structure. However, the transition between the negative and positive variations occurs at different depths: \( \sim 4 \text{ Mm} \) for the time-distance result, and \( \sim 5–8 \text{ Mm} \) for the ring-diagram inversions. It seems that this can be explained, at least in part, by differences in the sensitivity and resolution of the two methods (see Kosovichev et al. 2011).

Recently, Ilonidis et al. (2011) using the time-distance technique detected strong acoustic travel-time anomalies around 65 Mm (i.e., at 0.91 \( R_\odot \)) below the solar surface where a sunspot emerged 1 to 2 days later. These travel-time perturbations are an indication of sound-speed variations. In our simple model, \( \delta c^2/c^2 = 2.1 \times 10^{-4} \) at this depth. However, the observed signal lasts only for \( \sim 8 \text{ hr} \) and is not as strong in the layers immediately above the detected signal.

In conclusion, using acoustic mode frequencies observed by MDI/SOHO through most of solar cycle 23, we have estimated the sound-speed difference between solar maximum and minimum from 0.53 to 0.992 \( R_\odot \). The sound-speed difference seems to increase with radius from the base of the convection zone or above until 0.985 \( R_\odot \) (i.e., 10 Mm below the surface) at the second helium ionization zone. Closer to the surface, it decreases steeply with radius. It is zero at 0.990 \( R_\odot \) (i.e., at a depth of 7 Mm) and, at 0.992 \( R_\odot \) (or 5.5 Mm deep), \( \delta c^2/c^2 = -9.2 \times 10^{-4} \). The transition of the sound speed at solar maximum from larger to smaller than at solar minimum takes place at a similar depth as the transition of the sound speed below an active region from larger to smaller than at a quiet region obtained by ring-diagram analysis, suggesting that the sound-speed variation in the solar interior with solar cycle could be an overall effect of the active regions local perturbation, and not a global structure change with solar activity.

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