Thermal Effects in the dynamics of disordered elastic systems

S. Bustingorry\textsuperscript{a} A. B. Kolton\textsuperscript{a} A. Rosso\textsuperscript{b} W. Krauth\textsuperscript{c} T. Giamarchi\textsuperscript{d}

\textsuperscript{a}Centro Atómico Bariloche, 8400 S.C. de Bariloche, Argentina
\textsuperscript{b}CNRS; Univ. Paris-Sud, UMR 8626, ORSAY CEDEX, F-91405, LPTMS, France
\textsuperscript{c}CNRS-Laboratoire de Physique Statistique, Ecole Normale Supérieure, 24 rue Lhomond, 75231 Paris Cedex 05, France
\textsuperscript{d}DPMC-MaNEP, University of Geneva, 24 Quai Ernest Ansermet, 1211 Geneva 4, Switzerland

Abstract

Many seemingly different macroscopic systems (magnets, ferroelectrics, CDW, vortices,..) can be described as generic disordered elastic systems. Understanding their static and dynamics thus poses challenging problems both from the point of view of fundamental physics and of practical applications. Despite important progress many questions remain open. In particular the temperature has drastic effects on the way these systems respond to an external force. We address here the important question of the thermal effect close to depinning, and whether these effects can be understood in the analogy with standard critical phenomena, analogy so useful to understand the zero temperature case. We show that close to the depinning force temperature leads to a rounding of the depinning transition and compute the corresponding exponent. In addition, using a novel algorithm it is possible to study precisely the behavior close to depinning, and to show that the commonly accepted analogy of the depinning with a critical phenomenon does not fully hold, since no divergent lengthscale exists in the steady state properties of the line below the depinning threshold.

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tems. Given the success of the intuition gathered from the analogy with the critical phenomena, one is tempted to extend it to the case of finite temperature. In that case, thermal activation always allows to pass barriers ensuring a finite velocity at any force. Close to the depinning force \( F_c \), the finite temperature would thus be naively analogous to an external field (such as a finite magnetic field) coupling to the order parameter (e.g. the magnetization in a magnetic system) and ensuring that this parameter is finite on both sides of the transition. This analogy suggests immediately two important consequences: a) there must exist a rounding of the depinning transition due to the temperature and a thermal rounding exponent \( V(F_c) \sim T^\psi \), as for standard critical rounding; b) a divergent lengthscale must exist on both sides of the transition, and at “short” length-scales the system must resemble the “critical” system, while above this divergent length the system must reflect the corresponding fixed point (high or low temperature for a normal critical phenomenon, zero force or high force in the case of the depinning transition). These consequences for the finite temperature behavior are quite striking and of course of direct experimental relevance, since experiments are always performed at a finite temperature.

However, despite the success of the analogy with critical phenomena for \( T = 0 \), its extension to finite temperature is not guaranteed. It is thus important to check what remains of these properties. We address here these two points, and show that while a thermal rounding does indeed exist, there is no divergent lengthscale associated with the steady state properties of the line for \( F < F_c \), showing that the analogy with a standard critical phenomenon does not hold and making it a challenge to develop an intuitive picture of the depinning transition at finite temperatures.

2. Thermal rounding

We first concentrate on the question of thermal rounding.

Although analytical equations for the motion at finite temperature do exist \[10\] they are in practice very complicated to solve, and close to depinning no definite picture has emerged from them yet. However this question can be tackled by a numerical analysis of the equations of motion. We used a new technique allowing to avoid sample to sample fluctuations of the pinning force, which allowed us to obtain a very good statistics and to extract the depinning exponent. Details and further reference to previous studies of this problem in the literature can be found in Ref. \[17\]. Fig. 1 shows the steady state velocity of a system at the critical force.

Data shows a good scaling of the form \( v \sim T^\psi \), leading to the value \( \psi \approx 0.15 \). More importantly one could show by measuring the structure factor of the interface that both the thermally-rounded and the \( T = 0 \) depinning, display the same large-scale geometry, described by an identical divergence of a characteristic length \( \xi \) with the velocity of the form \( \xi \propto v^{-\nu/\beta} \), where \( \nu \) and \( \beta \) are respectively the \( T = 0 \) correlation and depinning exponents.

This remarkable fact fits very well universal scaling ideas from standard critical phenomena. It is important also to point out that so far there is no theoretical explanation of the value of the thermal rounding exponent (see Ref. \[17\] for a detailed discussion on that point). Quite paradoxically the best estimate seems to be provided by a direct application of the formula for static critical phenomena, which of course has no justification in the case of such dynamical transition. From a more fundamental point of view the scaling found above strongly suggests that the rounding of singularities that appear in the renormalization study of the depinning \[10\] are still controlled at finite temperatures by the velocity alone, as was the case for the \( T = 0 \) depinning.
The naive vision of the characteristic lengthscales and roughness of the line, in its moving frame. The analogy with critical phenomena would suggest a divergent lengthscale on both sides of the transition and a critical regime. This is in very different from what actually happens and is depicted in Fig. 3.

The analysis of thermal rounding would thus comfort the idea to extend the analogy with standard critical phenomena to finite temperatures. As we will see this is not the case when the characteristic lengthscales of the line are examined.

3. Characteristic lengthscales

A DES is characterized by a roughening exponent $\zeta$ that describes how the displacement from a flat configuration grow with the distance $L$ between two points $u(L) \sim L^\zeta$. For a line in a two dimensional space, three roughness exponents can be easily defined. The equilibrium roughness exponent corresponding to zero applied force is $\zeta_{eq} = 2/3$. If the line is moving very fast $F \gg F_c$ it averages over disorder and the system is thus equivalent to a pure thermal system. In one dimension, thermal fluctuations alone lead to a roughness exponent $\zeta_{th} = 1/2$. Finally, at zero temperature, if the line is right at the critical force, it is characterized by the roughness exponent $\zeta_{dep} \simeq 1.25$ [18]. The analogy with a standard critical phenomenon would thus suggest that an observation of the roughness of the line (in the moving frame in which the line is at rest) would lead to a divergent lengthscale on both side of the transition separating the various roughness regimes as depicted on Fig. 2. However this picture disagreed with a functional renormalization group analysis of the small force (creep) regime, that was suggesting that $\zeta_{eq}$ should be observed at short, not large lengthscales [16].

Given the difficulty to analyze this question analytically or by using the standard numerical algorithms (Langevin dynamics for example) due to the extremely long computational times needed close to the depinning, we developed a new algorithm to tackle such a problem. Details on the algorithm can be found in [19,20]. The basis idea is to use the fact that for very small temperatures, the system will spend most of its time in the configuration that has the largest escape barrier, since the escape time becomes infinitely longer than for all the other configurations. The steady state properties of the system are thus dominated by this particular configuration. This is the generalization for dynamics of the case of equilibrium thermodynamics where the partition function of the system is dominated at low temperatures by the ground state of the system. Our algorithm allows by enumeration to find such a configuration. Given the fact that the algorithm does not simulate the (extremely slow) dynamics close to the depinning, it can obtain quite quickly this configuration without suffering from the slowdown of the dynamics at low temperatures.

The results are sketched in Fig. 3. They show clearly that no divergent lengthscale exists in the steady state properties of the line for $F < F_c$, in direct contrast with a naive extrapolation of our intuition on standard critical phenomena. In order to check that this result was no an artefact or our algorithm and that no subtle inversion of limits $T \to 0$
and $F \to F_c$ could affect this result, we also spend considerable time recovering the crossover length by more conventional Langevin dynamics simulations. The results are shown in Fig. 3 and fully confirm the above results and the absence of divergent length-scale on the lower side of the transition.

These results clearly shows that the intuition based on standard critical phenomena should be taken with a grain of salt and poses the problem of the theoretical description of the depinning transition at finite temperatures. As for the case of the thermal rounding, although this information is in principle encoded in the FRG equations at finite temperature, extracting the physical behavior from these equations remain a very challenging task.

4. Conclusion

We have analyzed the effect of finite temperature on the depinning transition of a disordered elastic system. We have shown that at finite temperature the depinning transition is thermally rounded. The thermal rounding exponent $\psi \simeq 0.15$ needs a theoretical explanation, since for the moment the only formula which seems to fit quantitatively is an unjustified extrapolation of the static critical rounding exponents for a standard critical phenomena. Although the existence of thermal rounding would be in good agreement of the extrapolation of our intuition on critical phenomena to the depinning transition, we have also shown that the depinning transition is not accompanied by a divergent lengthscale for $F < F_c$ that would have bearings on the steady state properties of the line. This is in stark contrast with what happens in a normal critical phenomena, and directly prompts for a good description of the depinning transition.

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References

[1] S. Lemerle et al., Phys. Rev. Lett. 80, 849 (1998).
[2] M. Bauer et al., Phys. Rev. Lett. 94, 207211 (2005).
[3] M. Yamanouchi et al., Phys. Rev. Lett. 96, 096601 (2006).
[4] P. J. Metaxas et al., Phys. Rev. Lett. 99, 217208 (2007).
[5] P. Paruch, T. Giamarchi, and J. M. Triscone, Phys. Rev. Lett. 94, 197601 (2005).
[6] P. Paruch and J. M. Triscone, Appl. Phys. Lett. 88, 162907 (2006).
[7] S. Moulinet, A. Rosso, W. Krauth, and E. Rolley, Phys. Rev. E 69, 35103(R) (2004).
[8] E. Bouchaud et al., 50, 1703 (2002).
[9] M. Alava, P. K. V. Nukalaz, and S. Zapperi, Adv. Phys. 55, 349 (2006).
[10] G. Blatter et al., Rev. Mod. Phys. 66, 1125 (1994).
[11] X. Du et al., Nature Physics 3, 111 (2007).
[12] T. Nattermann and S. Brazovskii, Adv. Phys. 53, 177 (2004).
[13] T. Giamarchi, in Quantum phenomena in mesoscopic systems, edited by Italian Physical Society (IOS Press, Bologna, 2004), cond-mat/0403531.
[14] T. Giamarchi, A. B. Kolton, and A. Rosso, in Jamming, Yielding and Irreversible deformation in condensed matter, edited by M. C. Miguel and J. M. Rubi (Springer-Verlag, Berlin, 2006), p. 91, cond-mat/0503437.
[15] D. S. Fisher, Phys. Rev. B 31, 1396 (1985).
[16] P. Chauve, T. Giamarchi, and P. Le Doussal, Phys. Rev. B 62, 6241 (2000).
[17] S. Bustingorry, A. B. Kolton, and T. Giamarchi, Europhys. Lett. 81, 20005 (2007).
[18] A. Rosso, A. K. Hartmann, and W. Krauth, Phys. Rev. E 67, 21602 (2003).
[19] A. B. Kolton, A. Rosso, T. Giamarchi, and W. Krauth, Phys. Rev. Lett. 97, 057001 (2006).
[20] A. B. Kolton, A. Rosso, T. Giamarchi, and W. Krauth, in preparation.