Gated Feedback Recurrent Neural Networks

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Abstract
In this work, we propose a novel recurrent neural network (RNN) architecture. The proposed RNN, gated-feedback RNN (GF-RNN), extends the existing approach of stacking multiple recurrent layers by allowing and controlling signals flowing from upper recurrent layers to lower layers using a global gating unit for each pair of layers. The recurrent signals exchanged between layers are gated adaptively based on the previous hidden states and the current input. We evaluated the proposed GF-RNN with different types of recurrent units, such as tanh, long short-term memory and gated recurrent units, on the tasks of character-level language modeling and Python program evaluation. Our empirical evaluation of different RNN units, revealed that in both tasks, the GF-RNN outperforms the conventional approaches to build deep stacked RNNs. We suggest that the improvement arises because the GF-RNN can adaptively assign different layers to different timescales and layer-to-layer interactions (including the top-down ones which are not usually present in a stacked RNN) by learning to gate these interactions.

1. Introduction
Recurrent neural networks (RNN) have been widely studied and used for various machine learning tasks which involve sequence modeling, especially when the input and output have variable lengths. Recent studies have revealed that RNNs using gating units can achieve promising results in both classification and generation tasks (see, e.g., Graves, 2013; Bahdanau et al., 2014; Sutskever et al., 2014).

Although RNNs can theoretically capture any long-term dependency in an input sequence, it is well-known to be difficult to train an RNN to actually do so (Hochreiter, 1991; Bengio et al., 1994; Hochreiter, 1998). One of the most successful and promising approaches to solve this issue is by modifying the RNN architecture e.g., by using a gated activation function, instead of the usual state-to-state transition function composing an affine transformation and a point-wise nonlinearity. A gated activation function, such as the long short-term memory (LSTM, Hochreiter & Schmidhuber, 1997) and the gated recurrent unit (GRU, Cho et al., 2014), is designed to have more persistent memory so that it can capture long-term dependencies more easily.

Sequences modeled by an RNN can contain both fast changing and slow changing components, and these underlying components are often structured in a hierarchical manner. A conventional way to encode this hierarchy in an RNN has been to stack multiple levels of recurrent layers (Schmidhuber, 1992; El Hihi & Bengio, 1995; Graves, 2013; Hermans & Schrauwen, 2013). More recently, Koutnık et al. (2014) proposed a more explicit approach to partition the hidden units in an RNN into groups such that each group receives the signal from the input and the other groups at a separate, predefined rate, which allows feedback information between these partitions to be propagated at multiple timescales.

In this paper, we propose a novel design for RNNs, called a gated-feedback RNN (GF-RNN), to deal with the issue of learning multiple adaptive timescales. The proposed RNN has multiple levels of recurrent layers like stacked RNNs do. However, it uses gated-feedback connections from upper recurrent layers to the lower ones. This makes the hidden states across a pair of consecutive time-steps fully connected. To encourage each recurrent layer to work at different timescales, the proposed GF-RNN controls the strength of the temporal (recurrent) connection adaptively. This effectively lets the model to adapt its structure based on the input sequence.

We empirically evaluated the proposed model against the conventional stacked RNN and the usual, single-layer RNN on the task of language modeling and Python program eval-
2. Recurrent Neural Network

A recurrent neural network (RNN) is able to process a sequence of arbitrary length by recursively applying a transition function to its internal hidden state for each symbol of the input sequence. The activation of the hidden state at time-step $t$ is computed as a function $f$ of the current input symbol $x_t$ and the previous hidden state $h_{t-1}$:

$$ h_t = f(x_t, h_{t-1}). $$

(1)

It is common to use the state-to-state transition function $f$ as the composition of an element-wise nonlinearity with an affine transformation of both $x_t$ and $h_{t-1}$:

$$ h_t = \phi(Wx_t + Uh_{t-1}), $$

(2)

where $W$ is input-to-hidden weight matrix, $U$ is the state-to-state recurrent weight matrix, and $\phi$ is usually a logistic sigmoid function or a hyperbolic tangent function.

We can factorize the probability of a sequence of arbitrary length into

$$ p(x_1, \cdots, x_T) = p(x_1)p(x_2 | x_1) \cdots p(x_T | x_1, \cdots, x_{T-1}). $$

Then, we can train an RNN to model this distribution by letting it predict the probability of the next symbol $x_{t+1}$ given a hidden state vector $h_t$ which is a function of all the previous symbols $x_1, \cdots, x_{t-1}$ and current symbol $x_t$:

$$ p(x_{t+1} | x_1, \cdots, x_t) = g(h_t). $$

This approach of using a neural network to model a probability distribution over sequences is widely used, for instance, in language modeling (see, e.g., Bengio et al., 2001; Mikolov, 2012).

2.1. Gated Recurrent Neural Network

The difficulty of training an RNN to capture long-term dependencies has been known for long (Hochreiter, 1991; Bengio et al., 1994; Hochreiter, 1998). A previously successful approaches to this fundamental challenge has been to modify the state-to-state transition function to encourage some hidden units to adaptively maintain long-term memory, creating paths in the time-unfolded RNN, such that gradients can flow over many time-steps.

Long short-term memory (LSTM) was proposed by Hochreiter & Schmidhuber (1997) to specifically address this issue of learning long-term dependencies. The LSTM maintains a separate memory cell inside it that updates and exposes its content only when deemed necessary. More recently, Cho et al. (2014) proposed a gated recurrent unit (GRU) which adaptively remembers and forgets its state based on the input signal to the unit. Both of these units are central to our proposed model, and we will describe them in more details in the remainder of this section.

2.1.1. Long Short-Term Memory

Since the initial 1997 proposal, several variants of the LSTM have been introduced (Gers et al., 2000; Zaremba et al., 2014). Here we follow the implementation provided by Zaremba et al. (2014).

Such an LSTM unit consists of a memory cell $c_t$, an input gate $i_t$, a forget gate $f_t$, and an output gate $o_t$. The memory cell carries the memory content of an LSTM unit, while the gates control the amount of changes to and exposure of the memory content. The content of the memory cell $c_{t-1}^j$ of the $j$-th LSTM unit at time-step $t$ is updated similar to the form of a gated leaky neuron, i.e., as the weighted sum of the new content $c_t^j$ and the previous memory content $c_{t-1}^j$ modulated by the input and forget gates, $i_t^j$ and $f_t^j$, respectively:

$$ c_t^j = f_t^j c_{t-1}^j + i_t^j \tilde{c}_t^j. $$

(3)

where

$$ \tilde{c}_t = \text{tanh} (W_c x_t + U_c h_{t-1}). $$

(4)

The input and forget gates control how much new content should be memorized and how much old content should be forgotten, respectively. These gates are computed from the previous hidden states and the current input:

$$ i_t = \sigma(W_i x_t + U_i h_{t-1}), $$

(5)

$$ f_t = \sigma(W_f x_t + U_f h_{t-1}), $$

(6)

where $i_t = \left[ i_t^1 \cdots i_t^p \right]^T$ and $f_t = \left[ f_t^1 \cdots f_t^p \right]^T$ are respectively the vectors of the input and forget gates in a recurrent layer composed of $p$ LSTM units. $\sigma(\cdot)$ is an element-wise logistic sigmoid function. $x_t$ and $h_{t-1}$ are the input vector and previous hidden states of the LSTM units, respectively.

Once the memory content of the LSTM unit is updated, the hidden state $h_t^j$ of the $j$-th LSTM unit is computed as:

$$ h_t^j = o_t^j \text{tanh}(c_t^j). $$

The output gate $o_t^j$ controls to which degree the memory content is exposed. Similarly to the other gates, the output gate also depends on the current input and the previous hidden states such that

$$ o_t = \sigma(W_o x_t + U_o h_{t-1}). $$

(7)
In other words, these gates and the memory cell allow an LSTM unit to adaptively *forget, memorize* and *expose* the memory content. If the detected feature, i.e., the memory content, is deemed important, the forget gate will be closed and carry the memory content across many time-steps, which is equivalent to capturing a long-term dependency. On the other hand, the unit may decide to reset the memory content by opening the forget gate. Since these two modes of operations can happen simultaneously across different LSTM units, an RNN with multiple LSTM units may capture both fast-moving and slow-moving components.

### 2.1.2. Gated Recurrent Unit

The GRU was recently proposed by Cho et al. (2014). Like the LSTM, it was designed to adaptively reset or update its memory content. Each GRU thus has a reset gate $r^j_t$ and an update gate $z^j_t$ which are reminiscent of the forget and input gates of the LSTM. However, unlike the LSTM, the GRU fully exposes its memory content each time-step and balances between the previous memory content and the new memory content strictly using leaky integration, albeit with its adaptive time constant controlled by update gate $z^j_t$.

At time-step $t$, the state $h^j_t$ of the $j$-th GRU is computed by

$$h^j_t = (1 - z^j_t)h^j_{t-1} + z^j_t \tilde{h}^j_t,$$

where $h^j_{t-1}$ and $\tilde{h}^j_t$ respectively correspond to the previous memory content and the new candidate memory content. The update gate $z^j_t$ controls how much of the previous memory content is to be forgotten and how much of the new memory content is to be added. The update gate is computed based on the previous hidden state $h_{t-1}$ and the current input $x_t$:

$$z^j_t = \sigma (W_z x_t + U_z h_{t-1}),$$

where $z^j_t = \{z^j_k\}_{k=1}^p$. The new memory content $\tilde{h}^j_t$ is computed similarly to the conventional transition function in Eq. (2):

$$\tilde{h}^j_t = \tanh (W x_t + r^j_t \odot U h_{t-1}),$$

where $\tilde{h}^j_t = \{\tilde{h}^j_k\}_{k=1}^p$ and $\odot$ is an element-wise multiplication.

One major difference from the traditional transition function (Eq. (2)) is that the state of the previous step $h_{t-1}$ is modulated by the reset gates $r_t$. This behavior allows a GRU unit to ignore the previous hidden states whenever it is deemed necessary considering the previous hidden states and the current input:

$$r^j_t = \sigma (W_r x_t + U_r h_{t-1}).$$

The update mechanism helps the GRU to capture long-term dependencies. Whenever a previously detected feature, or the memory content is considered to be important for later use, the update gate will be closed to carry the current memory content across multiple time-steps. By using the reset mechanism, the RNN with the GRU units use the model capacity efficiently by allowing each GRU to reset whenever the detected feature is not necessary anymore.

### 3. Gated Feedback Recurrent Neural Network

Although capturing long-term dependencies in a sequence is an important and difficult goal of recurrent neural networks (RNN), it is worthwhile to notice that a sequence often consists of both slow-moving and fast-moving components, of which only the former corresponds to long-term dependencies. Ideally, an RNN needs to capture both long-term and short-term dependencies.

El Hihi & Bengio (1995) first showed that an RNN can capture these dependencies of different timescales more easily and efficiently when the hidden units of the RNN is explicitly partitioned into groups that correspond to different timescales. The clockwork RNN (CW-RNN) (Koutnık et al., 2014) implemented this by allowing the $i$-th module to operate at the rate of $2^{i-1}$, meaning that the module is updated only when $t \mod 2^{i-1} = 0$. This makes each module to operate at different rates. In addition, they precisely defined the connectivity pattern between modules by allowing the $i$-th module to be affected by $j$-th module when $j > i$.

Here, we propose to generalize the CW-RNN by allowing the model to adaptively adjust the connectivity pattern between the hidden layers in the consecutive time-steps. Similar to the CW-RNN, we partition the hidden units into multiple modules in which each module corresponds to a different layer in a stack of recurrent layers.

Unlike the CW-RNN, however, we do not set an explicit rate for each module. Instead, we let each module operate at different timescales by hierarchically stacking them. Each module is fully connected to all the other modules across the stack and itself. In other words, we do not define the connectivity pattern across a pair of consecutive time-steps. This is contrary to the design of CW-RNN and the conventional stacked RNN. The recurrent connection between two modules, instead, is gated by a logistic unit $([0, 1])$ which is computed based on the current input and the previous states of the hidden layers. We call this gating unit a *global reset* gate, as opposed to a unit-wise reset gate which applies only to a single unit (See Eqs. (3) and (10)).
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Figure 1. Illustrations of (a) conventional stacking approach and (b) gated-feedback approach to form a deep RNN architecture. Bullets in (b) correspond to global reset gates. Skip connections are omitted to simplify the visualization of networks.

The global reset gate is computed as:

\[ g_i^j = \sigma \left( w_i^{i \rightarrow j} h_i^{j-1} + u_i^{i \rightarrow j} h_{i-1}^{j-1} \right), \tag{12} \]

where \( L \) is the number of hidden layers, \( w_i^{i \rightarrow j} \) and \( u_i^{i \rightarrow j} \) are the weight vectors for the input and the hidden states of all the layers at time-step \( t - 1 \), respectively. For \( j = 1 \), \( h_i^{j-1} = x_t \).

The global reset gate \( g_i^j \) is applied collectively to the signal from the \( i \)-th layer \( h_{i-1}^{j} \) to the \( j \)-th layer \( h_i^j \). In other words, the signal from the layer \( i \) to the layer \( j \) is controlled based on the input and the previous hidden states.

Fig. 1 illustrates the difference between the conventional stacked RNN and our proposed GF-RNN. In both models, information flows from lower layers to upper layers, respectively, corresponding to finer timescale and coarser timescale. The GF-RNN, however, further allows information from the upper recurrent layer, corresponding to coarser timescale, flows back into the lower layers, corresponding to finer timescales.

We call this RNN with a fully-connected recurrent transition and global reset gates, a **gated-feedback RNN** (GF-RNN). In the remainder of this section, we describe how to use the previously described LSTM unit, GRU, and more traditional \( \tanh \) unit in the GF-RNN.

### 3.1. Practical Implementation of GF-RNN

#### 3.1.1. \( \tanh \) Unit

For a stacked \( \tanh \)-RNN, the signal from the previous time-step is gated. The hidden state of the \( j \)-th layer is computed by

\[ h_i^j = \tanh \left( W_i^{j-1 \rightarrow j} h_i^{j-1} + \sum_{i=1}^{L} g_i^{i \rightarrow j} U_i^{i \rightarrow j} h_{i-1}^{i-1} \right), \]

where \( W_i^{j-1 \rightarrow j} \) and \( U_i^{i \rightarrow j} \) are the weight matrices of the incoming connections from the input and the \( i \)-th module, respectively. Compared to Eq. (2), the only difference is that the previous hidden states are controlled by the global reset gates.

#### 3.1.2. Long Short-Term Memory and Gated Recurrent Unit

In the cases of LSTM and GRU, we do not use the global reset gates when computing the unit-wise gates. In other words, Eqs. (5)–(7) for LSTM, and Eqs. (9) and (11) for GRU are not modified. We only use the global reset gates when computing the new state (see Eq. (4) for LSTM, and Eq. (10) for GRU).

The new memory content of an LSTM at the \( j \)-th layer is computed by

\[ \tilde{c}_i^j = \tanh \left( W_c^{j-1 \rightarrow j} h_i^{j-1} + \sum_{i=1}^{L} g_i^{i \rightarrow j} U_c^{i \rightarrow j} h_{i-1}^{i-1} \right). \]

In the case of a GRU, similarly,

\[ \tilde{h}_i^j = \tanh \left( W_i^{j-1 \rightarrow j} h_i^{j-1} + r_i^j \odot \sum_{i=1}^{L} g_i^{i \rightarrow j} U_i^{i \rightarrow j} h_{i-1}^{i-1} \right). \]

### 4. Experiment Settings

#### 4.1. Tasks

We evaluated the proposed gated-feedback RNN (GF-RNN) on character-level language modeling and Python
program evaluation. Both tasks are representative examples of discrete sequence modeling, where a model is trained to minimize the negative log-likelihood of training sequences:

$$\min_{\theta} \frac{1}{N} \sum_{n=1}^{N} \sum_{t=1}^{T_n} - \log p \left( x_t^n \mid x_t^{n-1}, \ldots, x_{t-1}^{n-1}; \theta \right),$$

where $\theta$ is a set of model parameters.

### 4.1.1. LANGUAGE MODELING

We used the dataset made available as a part of the human knowledge compression contest (Hutter, 2012). We refer to this dataset as the *Hutter dataset*. The dataset, which was built from English Wikipedia, contains 100 MBytes of characters which include Latin alphabets, non-Latin alphabets, XML markups and special characters. Closely following the protocols in (Mikolov et al., 2012; Graves, 2013), we used the first 90 MBytes of characters to train a model, the next 5 MBytes as a validation set, and the remaining as a test set, with the vocabulary of 205 characters including a token for an unknown character. We used the average number of bits-per-character (BPC, $E[-\log_2 P(x_t \mid h_t)]$) to measure the performance of each model on the Hutter dataset.

### 4.1.2. PYTHON PROGRAM EVALUATION

Zaremba & Sutskever (2014) recently showed that a recurrent neural network, more specifically a stacked LSTM, is able to execute a short Python script. Here, we compared the proposed architecture against the conventional stacking approach model on this task, to which refer as *Python program evaluation*.

Scripts used in this task include addition, multiplication, subtraction, for-loop, variable assignment, logical comparison and if-else statement. The goal is to generate, or predict, a correct return value of a given Python script. The input is a program while the output is the result of a print statement. Both the input script and the output are sequences of characters, where the input and output vocabularies respectively consist of 41 and 13 symbols.

The advantage of evaluating the models with this task is that we can artificially control the difficulty of each sample (input-output pair). The difficulty is determined by the number of nesting levels in the input sequence and the length of the target sequence. We can do a finer-grained analysis of each model by observing its behavior on examples of different difficulty levels.

### 4.2. Models

We compared three different RNN architectures: a single-layer RNN, a stacked RNN and the proposed GF-RNN. For each architecture, we evaluated three different transitions functions: tanh + affine, long short-term memory (LSTM) and gated recurrent unit (GRU). For fair comparison, we constrained the number of parameters of each model to be roughly similar to each other.

For each task, in addition to these capacity-controlled experiments, we conducted a few extra experiments to further test and better understand the properties of the GF-RNN.

#### 4.2.1. LANGUAGE MODELING

For the task of character-level language modeling, we constrained the number of parameters of each model to correspond to that of a single-layer RNN with 1000 tanh units (see Table 1 for more details.) Each model is trained for at most 100 epochs.

We used RMSProp (Hinton, 2012) and momentum to tune the model parameters (Graves, 2013). According to the preliminary experiments and their results on the validation set, we used a learning rate of 0.001 and momentum coefficient of 0.9 when training the models having either GRU or LSTM units. It was necessary to choose a much smaller learning rate of $5 \times 10^{-5}$ in the case of tanh units to ensure the stability of learning. Whenever the norm of the gradient explodes, we halve the learning rate.

Each update is done using a minibatch of 100 subsequences of length 100 each, to avoid memory overflow problems when unfolding in time for backprop. We approximate full back-propagation by carrying the hidden state computed at the previous update to initialize the hidden units in the next update. After every 100-th update, the hidden states were reset to all zeros.

| Unit          | Architecture | # of Units                  |
|---------------|--------------|-----------------------------|
| tanh          | Single       | $1 \times 1000$            |
|               | Stacked      | $3 \times 390$            |
|               | Gated Feedback | $3 \times 303$            |
| GRU           | Single       | $1 \times 540$            |
|               | Stacked      | $3 \times 228$            |
|               | Gated Feedback | $3 \times 165$            |
|               | Gated Feedback L | $3 \times 228$            |
| LSTM          | Single       | $1 \times 456$            |
|               | Stacked      | $3 \times 191$            |
|               | Gated Feedback | $3 \times 140$            |
|               | Gated Feedback L | $3 \times 191$       |
**Table 2.** Test set BPC of models trained on the Hutter dataset for a 100 epochs. (⋆) We did not train Gated Feedback L models with tanh units.

|                  | tanh | GRU  | LSTM |
|------------------|------|------|------|
| Single-layer     | 1.937| 1.883| 1.887|
| Stacked          | 1.892| 1.871| 1.868|
| Gated Feedback   | 1.949| 1.855| 1.842|
| Gated Feedback L | N/A* | 1.813| 1.789|

### 4.2.2. Python Program Evaluation

For the task of Python program evaluation, we used an RNN encoder-decoder based approach to learn the mapping from Python scripts to the corresponding outputs as done by Cho et al. (2014); Sutskever et al. (2014) for machine translation. When training the models, Python scripts are fed into the encoder RNN, and the hidden state of the encoder RNN is unfolded for 50 time-steps. Prediction is performed by the decoder RNN whose initial hidden state is initialized with the last hidden state of the encoder RNN. The first hidden state of encoder RNN $h_0$ is always initialized to a zero vector.

For this task, we used GRU and LSTM units either with or without the gated-feedbacks. We constrained the number of parameters to 2.4M to control the capacity of each model (each encoder or decoder RNN has three hidden layers with 200 units).

Following Zaremba & Sutskever (2014), we used the *mixed* curriculum strategy for training each model, where each training example has a random difficulty sampled uniformly. We generated 320,000 examples using the script provided by Zaremba & Sutskever (2014), with the nesting randomly sampled from $[1, 5]$ and the target length from $[1, 10^10]$.

We used Adam (Kingma & Ba, 2014) to train our models, and each update was using a minibatch with 128 sequences. We used a learning rate of 0.001 and $\beta_1$ and $\beta_2$ were both set to 0.01. We trained each model for 30 epochs, with early stopping based on the validation set performance to prevent over-fitting.

At test time, we evaluated each model on multiple sets of test examples where each set is generated using a fixed target length and number of nesting levels. Each test set contains 2,000 examples which are ensured not to overlap with the training set.

### 5. Results and Analysis

#### 5.1. Language Modeling

It is clear from Table 2 that the proposed gated-feedback architecture outperforms the other baseline architectures that we have tried when used together with widely used gated units such as LSTM and GRU. However, the proposed architecture failed to improve the performance of a vanilla-RNN with tanh units. In addition to the final modeling performance, in Fig. 2, we plotted the learning curves of some models against wall-clock time (measured in seconds). RNNs that are trained with the proposed gated-feedback architecture tends to make much faster progress over time. This behavior is observed both when the number of parameters is constrained and when the number of hidden units is constrained. This suggests that the proposed GF-RNN significantly facilitates optimization/learning.
Table 3. Generated texts with our trained models. Given the seed at the left-most column (bold-faced font), the models predict next 200 ∼ 300 characters. Tabs, spaces and new-line characters are also generated by the models.

| Seed | Stacked LSTM | GF-LSTM |
|------|--------------|---------|
| [[pl:Icon]] | <revision> | <revision> |
| [[pt:Icon]] | <timestamp> | <timestamp> |
| [[ru:Icon]] | 2002-07-20T18:33:34Z | 2006-09-03T11:38:06Z |
| [[sv:Programspraket Icon]] | <contributor> | <contributor> |
| <username>The Courseichi</username> | <username>Navlab</username> |
| vehicles in [[jenguit]]. | | |
| ==The inhibitors and alphabetxy and moral/ | ==The increase from the time |
| hands in---in four [[communications]] and | |
| | |

Effect of Global Reset Gates

After observing the superiority of the proposed gated-feedback architecture over the conventional single-layer or stacked ones, we further trained another GF-RNN with LSTM units, but this time, after fixing the global reset gates to 1 to validate the need for the global reset gates. Without the global reset gates, feedback signals from the upper recurrent layers influence the lower recurrent layer fully without any control.

In Fig. 3, it can be seen that this omission of the global reset gates hurts the performance (cyan) compared to the one with the global reset gates (magenta). The test set BPC of GF-LSTM without global reset gates was 1.854.

![Figure 3. Validation learning curves of the stacked LSTM, GF-LSTM with the global reset gates and GF-LSTM without them. Best viewed in colors.](image)

Here we qualitatively evaluate the stacked LSTM and GF-LSTM trained earlier by generating text. We choose a sub-sequence of characters from the test set and use it as an initial seed. Once the model finishes reading the seed text, we let the model generate the following characters.

Table 3 shows the initial seeds and results of text generation. We observed that the stacked LSTM failed to close the tags with <username> and </username> in both trials. However, the GF-LSTM succeeded to close both of them, which shows that it learned about the structure of XML tags.

Table 4. Test set BPC of neural language models trained on the Hutter dataset, MRNN = multiplicative RNN results from Sutskever et al. (2011) and Stacked LSTM results from Graves (2013).

| MRNN | Stacked LSTM | GF-LSTM |
|------|--------------|---------|
| 1.60 | 1.67 | 1.58 |

Large GF-RNN

We trained a larger GF-RNN that has five recurrent layers, each of which has 700 LSTM units. This makes it possible for us to compare the performance of the proposed architecture against the previously reported results using other types of RNNs. In Table 4, we present the test set BPC by a multiplicative RNN (Sutskever et al., 2011), a stacked LSTM (Graves, 2013) and the GF-RNN with LSTM units. The performance of the proposed GF-RNN is comparable to, or better than, the previously reported best results. Note that Sutskever et al. (2011) used the vocabulary of 86 characters (removed XML tags and the Wikipedia markups),...
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5.2. Python Program Evaluation

Fig. 4 presents the test results of each model represented in heatmaps. The accuracy tends to decrease by the growth of target length or nesting, where the difficulty or complexity of the Python program increases. We observed that in the most of the test sets, GF-RNNs are outperforming Stacked RNNs, regardless of the type of units. In Fig. 4-(c), the red and yellow colors which indicate large gains are concentrated on top or right regions (either nesting or target length increases). It shows that GF-RNN is actually doing even better (relatively speaking) when the number of nesting grows or the length of target increases, and this implies that it outperforms especially when input sequences are more complicated.

6. Conclusion

We proposed a novel architecture for deep stacked RNNs which uses gated-feedback connections between different layers. Our experiments focused on challenging sequence modeling tasks of character-level language modeling and Python program evaluation. The results were consistent over different datasets, and clearly demonstrated that gated-feedback architecture is helpful when the models are trained on complicated sequences that involve long-term dependencies. We also showed that gated-feedback architecture was faster in wall-clock time over the training and achieved better performance compared to standard stacked RNN with a same amount of capacity. Large GF-LSTM was able to outperform the previously reported best results on character-level language modeling. This suggests that GF-RNNs are also scalable. GF-RNNs were able to outperform standard stacked RNNs on Python program evaluation task with varying difficulties.

Gated-feedback connection is a simple extension over the standard stacked RNNs, but it was able to show significant improvements on our benchmark and control experiments.

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Text Generation

Hutter dataset is often referred as a benchmark for character-level language modeling (Sutskever et al., 2011; Graves, 2013). In this supplementary material, we provide some samples generated by the gated-feedback RNN with LSTM units which was trained on Hutter dataset. We sampled once from the model (except the last sample) after providing a seed sequence extracted from the test set which was not used for training the model. We use bold-faced font whenever the following (generated) characters are considered highly relevant to the context of earlier seed text. We use red color to distinguish the seed text snippet from the generated one.

Sample #1

England, Italy, France, Germany and others.

==Euroscepticism in the United Kingdom==

Humbert and Colombi

* [[Royal Charlemagne|Crown Union of the Eastern Radio Silver Station]]

(T19 AD) explodes almost do train open in reaction to do not form dry oil. This is an essential implication of [posttransistor] that is significantly assumes modification of question. For example, it does not entail a being with a lower case, and declared they all in "The Glorification of Touchuff" [(2005 in literate press|prethis version)] was of the progress of (Vhersi')'. A top ranking of the decades was the beginning of Pulham [(Dan Delisa)] to put the a contract that could become a minimal operating system in common law. Membership however, stems Brussels struggles to conduct a museum] of this national lands are explicated in all groups, especially in traditional Ukrainian monetary values.

Sample #2

In Europe, Paris was the center stage for the [[French Revolution]], and it became an important centre of finance, commerce, and Funding important. The markets for the Union also include the invention of money lower and funding important.

Sample #3

Istanbul is located in north-western [[Turkey]] and south-eastern Europe within the [[Marmara Region]] on a total area of 400km² andwards by merging the airport and carry [[Discount of Cuba|Year of Empire|Temastique]],quot; "considered" (secret). [[Notable extreme points of North America]] (nut, because it were trooped by broken versions of him with either the Polish album by the U.S. Attorney's [[London Eye]] was problematic of clarified and even translated, in it among [[Britain]], the Basque Parliament can be assigned a new [[Austrodean]]

Damascus is also champions some years. He apparently failed to cover wrongdoing, Hamming Khan Atanahorn] of Lestergompolis of the Tropic of Churches to the undemocratism with lieutenants as Spoiler of the Union of the Honored Matres, Bulgaria had to proilmes mounted undrinks something instead of the brother, being green and blue. The [[Russia collapse|race]] received an estimated reconstructive tension between the Pacific Ocean and the island of [[Northumbria]], which are less than original Habsburg fast deficits. These are under [[Louise XIV of France|Louis XIV of France]] and again drove the city from Rome.

Sample #4

Google was founded by [[Larry Page]] and [[Sergey Brin]] while they were [[Doctor of Philosophy]] students at [[Stanford University]]. Together they own about 14,000 files filmer(266) [[January 15|15]] [[January 12|12]] [[January 1]].

Leading the democratization of the Czech Republic in 1948, the descendants of [[Charlotte of the Hanseatic Council]] were trophy in the House of Lords, begun as wives in [[North Africa]], [[Silicy]], [[Spanish Islam Mary]], [[Africa]] eeence (15,401) in 1949. Brown was vigorously implied of position with some demonstration of angels existed by merry with individuals that not yet be seen on the naked surname Grigorius titled "On by Kroizan Islam, the husband of Apis also the process of deriving opposites octa, to Govermental Discovery and Health Statistics.

Sample #5

Sample #6

Wikipedia

* [http://www.indianaJones.com/ IndianaJones.com; the official Indiana Jones site]
* [http://www.chesralder.net Theralder.net; the primary fan site of the series]
* [http://indianajones.wikicities.com The Indiana Jones Wiki]
* [http://www.thindywaxperience.com The Indy Experience]
* [http://www.indygeek.org/ Emagic]].

which presumably includes an inside Liberals or Civilian leader JHOC President. Two large faculty alien colonies led by Thomas Coit fit of Heracles who lives with Menander, Zeus, has a world ticket. Officially there is another Challenge to the Queen's Law for all possessions.) There is often no relevant]) and weapons systems. *
+ *[C Implementation for League Championship (novel)|The Edgar, feather-and-chestglum.shtml (see below)] during the head and the feast day and/or use of mud, degueus (knife), [[doucail]], [[tuna]]
Sample #7

== Disadvantages of IMAP ==

- IMAP is a very heavy and complicated protocol. Writing your own custom implementation of an IMAP server is of at least 20 orders of magnitude more complicated than a POP3 implementation. Client implementations are also much more complicated.

- Due to its capabilities, mythology’s possibility is still incomplete. Commentators on epistemic definitions typical of the past fall short of ethical altruism limit, arguing that the delegation should not be appropriate to oppress it, without expressive our knowledge about free market activities, as well as some – it is possible to check the limits on Wikipedia.

Put in direct film video – Advance Australia

Sample #8

* [[Christianity|Christian]] — 82%  
  ** [[Baptist]] — 15%  
  *** [[Methodism|Methodist]] — 10%  
  **** [[Church of Christ]] — 6%  
  *** [[Reformed Egyptian|Egyptian]] — 11%  
  ** [[Princeps senatus]] (or Archipelago for acids in the use of neutron species.) Long as a result of TLDs in the DNA of a large endometer. In this sense the electron shell structure densitises these &quot;molecular systems&quot;.

The mere density, and once (implying that, in most sense, deemed political or social evidence.)

-- See also --

* `''Chechen'' [des of the Prolog-Answer]'' [1952]]  
  [ubc., #99 - PVF version]  
  `''Concrete Principles of Closed Life in Philosophy 1900-1960'' (1992) ISBN 0689725942 ([NASA]) only to the `''International Union''). Since his works like `''[London Mathers]'' and `''[Last Labor Day]''.

The members of the royal family were in the middle age Linux, the standard execution signal was the compiler whose logo contained symbols for the [[Microsoft Windows release|Windows Network]] (Windows) and [[Access Internet Computers|ICA]] listing.

Sample #9

[[[Canada]], [[England]], [[France]], [[Missouri]]], revised as a symbol of past humans more controversial after having criticised the trend ended in breeding and protecting various categories. `''Antiqui'' marked the beginning of the epistle to Marian: &quot;tell me that it may, to make pre-remaining neighbours?quot; The need to reconcile you to the details of belief in datura, and talk about it in the appendix to his knowledge and not in any other manner.&quot;

Latter-day Saints with an essential equation have the corresponding reference for the time, if the acceleration oured a centuries-CLs ([Hitachi, Ltd.|Little Hitchcock]])

Sample #10

The meaning of life is subject to rights in [[economics]] and to generalize the inquiry on liberal liberals in real-life [[revolution]].

Leibniz believed in warming inestamp.