Using low dose x-ray speckle visibility spectroscopy to study dynamics of soft matter samples

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Abstract
We demonstrate the successful application of x-ray speckle visibility spectroscopy (XSVS) experiments to study the dynamics of radiation sensitive, biological samples with unprecedented small x-ray doses of 45 Gy and below. Using XSVS, we track the dynamics of casein micelles in native, concentrated, and acidified solution conditions, while substantially reducing the deposited dose as compared to alternative techniques like sequential x-ray photon correlation spectroscopy. The Brownian motion in a skim milk sample yields the hydrodynamic radius of the casein micelles while deviations from Brownian motion with a characteristic q-dependent diffusion coefficient \( D(q) \) can be observed in more concentrated solution conditions. The low dose applied in our experiments allows the observation of static, frozen speckle patterns from gelled acidic milk. We show that the XSVS technique is especially suitable for tracking dynamics of radiation sensitive samples in combination with the improved coherent properties of new generation x-ray sources, emphasizing the great potential for further investigations of protein dynamics using fourth generation synchrotrons and free electron lasers.

1. Introduction

X-ray photon correlation spectroscopy (XPCS) provides access to a hierarchy of spatial and temporal information with the exciting outlook of extending the application of biological small-angle x-ray scattering (Bio-SAXS) experiments considerably [1–4] by adding dynamical information. As a coherent scattering technique, XPCS will especially benefit from highly coherent x-ray sources such as 4th generation synchrotron storage rings and MHz x-ray free-electron lasers [5–10]. Thus, Bio-XPCS methods bear the potential of time-resolved investigations of processes relevant to biological function such as aggregation, phase separation, partitioning, and self-assembly, which are important for understanding for instance neurodegenerative diseases, the development of tissues and organs, virus infections, the formation of bio-inspired materials and many more. Moreover, studying dynamics in crowded biological systems can provide fundamental insight into protein interactions in concentrated environments [11, 12] advancing our microscopic understanding of processes such as misfolding and aggregation related to pathological cases such as Alzheimer’s and prion diseases. It can also help in the design and implementation of improved protein-based therapeutics with tailored transport and storage properties.

While the science case of Bio-XPCS is compelling, the technical challenges of realizing such experiments are considerable with radiation damage being one of the main obstacles when using highly intense x-ray beams. Atomic scale XPCS experiments, for example, apply x-ray doses of up to MGy and beyond, which...
can lead to beam-induced dynamics even in hard-condensed-matter samples [13–15]. Soft and biological matter samples are much more sensitive to radiation damage requiring continuous flowing [1, 16, 17] or scanning of the samples [18] with optimized data-taking strategies [19]. Typical critical x-ray doses for protein molecules in solution range from 7–10 kGy (BSA) to 0.3 kGy (RNase) after which a degradation of the SAXS patterns is visible [20]. These doses are easily reached within milliseconds when using focused beams of modern synchrotron sources.

In order to overcome this bottleneck of radiation damage, adapted experimental XPCS schemes such as serial x-ray speckle visibility spectroscopy (XSVS) [21–24] are needed, which allow to make full use of the increased brilliance and coherence of the new x-ray sources. An additional advantage of XSVS is that the temporal resolution is given by the single frame exposure time and not by the frame rate as in XPCS, therefore having less stringent requirements to the readout speed of pixelated x-ray detectors.

Here, we demonstrate the feasibility of measuring dynamics in biological systems with ultra low dose XSVS experiments. We make use of short exposure times and measure the dynamics of casein micelles with a maximum applied x-ray dose of 0.045 kGy only. This dose is orders of magnitude below damage thresholds reported for many monomeric proteins. Additionally, the results allow us to estimate the feasibility of Bio-XSVS experiments for a larger variety of proteins on a wide range of length scales.

2. Low dose coherent x-ray scattering experiments

The experiments were performed at the coherent applications beamline P10, PETRA III, DESY, Hamburg and at the time-resolved (U-)SAXS beamline ID02, ESRF, France [25]. The casein micelle samples were derived from commercial skim milk powder (SUCOFIN), and used without further purification. Residual aggregates and lipids were removed by centrifugation. A ‘native’ sample was prepared following the supplier’s instruction, resulting in a final casein micelles concentration of about 3 wt%.

The scattered intensity was recorded with two different versions of the EIGER photon counting detector [26–28]. Structural information can be obtained by azimuthally integrating the scattered intensity on the detector. The obtained scattering intensity \( I(q) \), with \( q = 4\pi \sin(\theta)/\lambda \) designating the modulus of the scattering vector, the wavelength \( \lambda \) and the scattering angle \( 2\theta \), contains information about the size, shape and size distribution of the scattering entities in the sample. The shape of the scattering particles is given by the single particle form factor \( P(q) \), which in the simple case of spheres with a homogeneous scattering density and radius \( R \) is

\[
P(q) = \left( \frac{3\sin(qR) - qR \cos(qR)}{(qR)^3} \right)^2.
\]

An additional modulation (speckle) of the scattered intensity can be observed for coherent scattering experiments, when the coherence volume of the incident radiation becomes comparable to the scattering volume. This speckle pattern depends on the spatial arrangement of the scatterers and therefore dynamical information can be obtained from the temporal evolution of the speckle pattern.

The size of the speckles on the detector can be estimated as \( S = \frac{\lambda}{2a} \) with \( a \) being the x-ray spot size on the sample and \( L \) the sample-detector-distance. To minimize the absorbed dose, the measurements were performed with comparably large \( a \), which consequently requires large \( L \) to resolve the speckles on the detector. A more detailed discussion about the best compromise between speckle contrast and dose can be found in [2]. A summary of the experimental parameters used in this study is given in table 1.

2.1. Speckle visibility spectroscopy in the low count regime

In standard XPCS experiments, sequential acquisitions from the same sample spot are measured, so that the intermediate scattering function \( g_2(q, t) \) (ISF) can be calculated from the scattered intensity \( I(\vec{q}) \) as

\[
g_2(q, t') = \frac{\langle I(\vec{q}, t)I(\vec{q}, t + t') \rangle}{\langle I(\vec{q}) \rangle^2} = 1 + \beta_0 |g_1(q, t')|^2,
\]

with \( \beta_0 \) being the speckle contrast. The time delay between two consecutive time frames is denoted \( t' \) and \( \langle \ldots \rangle \) is the ensemble average over all equivalent delay times \( t \) and pixels within a certain range of the absolute value \( |\vec{q}| \).

In order to reduce the deposited dose on a single spot of the sample as much as possible, we aim at obtaining the same dynamic information from single acquisitions. As the speckle contrast \( \beta \) depends on the exposure time \( \tau \) and the ISF of the sample like [29]

\[
\beta(q, \tau) = 2\frac{\beta_0}{\tau} \int_0^\tau (1 - t'/\tau)|g_1(q, t')|^2 \, dt',
\]

Before the ESRF-EBS upgrade.
Table 1. Experimental setups for low dose coherent x-ray scattering experiments.

| Beamline       | P10, DESY | ID02, ESRF |
|----------------|-----------|------------|
| Detector       | Dectris Eiger 4M | PSI Eiger 500k |
| Frame rate     | 750 Hz    | 22 kHz    |
| Sample-detector-distance L | 21.3 m | 30.7 m |
| Wavelength λ   | 1.54 Å    | 0.995 Å   |
| Beamsize \((a \times a)\) | \(\approx 60 \, \mu m \times 60 \, \mu m\) | \(\approx 30 \, \mu m \times 30 \, \mu m\) |
| Flux           | \(\approx 2 \times 10^{10} \, \text{ph s}^{-1}\) | \(\approx 4 \times 10^{10} \, \text{ph s}^{-1}\) |
| \(\beta_0\)    | \(\approx 23\%\) | \(\approx 28\%\) |
| \(q\)-range    | \(2.5 \times 10^{-3} \, \text{nm}^{-1}\) to \(-2 \times 10^{-4} \, \text{nm}^{-1}\) | \(1.5 \times 10^{-3} \, \text{nm}^{-1}\) to \(-2 \times 10^{-4} \, \text{nm}^{-1}\) |

Figure 1. (Left) Probabilities \(P(k)\) of measuring \(k = 0, 1\) or 2 photons at a fixed exposure time of \(\tau = 1.35 \, \mu s\) and at a scattering vector \(q = (6 \pm 2) \times 10^{-3} \, \text{nm}^{-1}\), which translates into a region of 1230 pixels on the detector (at beamline P10 with 21 m sample-to-detector distance, native casein micelle solution). The incident intensity was varied between \(2 \times 10^{8} \, \text{ph s}^{-1}\) and \(2 \times 10^{10} \, \text{ph s}^{-1}\) and the data was corrected following [31]. Each data point is calculated as the mean of 86 single acquisitions with closely matching \(<k>\). The solid lines represent the Poisson–gamma distribution, with a contrast \(\beta = 0.24\). (Right) Resulting contrast values, calculated following equation (4). The contrast value \(\beta\) is obtained as a weighted average and displayed as a solid line. The uncertainty of the fit is displayed as a dashed line band.

one can probe the properties of the ISF from a series of single frame acquisitions by varying the exposure time.

The speckle contrast for each acquisition can be calculated from a statistical analysis of the photon counts. Following the negative-binomial distribution [30], also known as the Poisson–gamma distribution, the speckle contrast can be obtained from the probabilities \(P(k)\) of pixels within an ensemble measuring \(k = 0, 1, 2\ldots\) photons as

\[
\beta = \frac{P(0)}{P(1)} - \frac{1}{<k>},
\]

with \(<k>\) denoting the mean number of photons per pixel per acquisition. The error in determining the contrast is given by [19]

\[
\Delta \beta = \frac{1}{<k>} \sqrt{\frac{2(1 + \beta)}{n_{\text{pix}} n_{\text{im}}}},
\]

with \(n_{\text{pix}}\) the number of pixel in the region of interest and \(n_{\text{im}}\) the number of frames. Determining the speckle contrast with high accuracy is the main difficulty of XSVS experiments with very low count rates (\(<k> < 10^{-2}\)). Therefore, extensive characterization of the experimental setup was performed before the experiments using porous silica glass (VYCOR) as a static sample. The characterizations were published in [31] and will not be repeated here. Substantial deviations in the measured photon statistics from those of the expected Poisson–gamma distribution at low count rates were found for both types of EIGER detectors used for this experiment. Due to this non-ideal behavior, we developed a detector correction scheme, which is explained as well in [31]. Performing this correction is mandatory for the experiments to work and was applied to all measurements in the following.
A corrected data set of a native casein micelle sample is displayed in figure 1, where the incident intensity was varied by using silicon attenuators. This illustrates the obtainable SNR as a function of coherent flux. Additionally, the fact that the measured contrast is independent of the incident intensity (at fixed exposure time) verifies the correction scheme as well as the absence of radiation damage effects. On the left-hand side, the probability $P(k)$ of measuring $k = 0, 1$ or 2 photons is plotted as a function of mean scattered intensity per pixel $\langle k \rangle$. The resulting speckle contrast is calculated for each triplet of $\langle k \rangle$ values, following equation (4), with the error following equation (5) (figure 1, right). The final $\beta(q, \tau)$ is calculated as a weighted average of the single data points and displayed as solid blue line, with dashed lines representing the statistical uncertainties stemming from the weighted average calculation. It can be clearly seen that with increasing mean intensity $\langle k \rangle$ the statistical error of $\beta$ reduces significantly. Therefore, the number of acquired images ($n_{im}$) was adapted in the following for each exposure time according to the obtained mean intensity $\langle k \rangle$. Additionally, the beam attenuation was adapted, in order to avoid exceeding a deposited dose of 45 Gy per acquisition. As can be seen from equation (5), in order to preserve the statistical accuracy of the speckle contrast, a reduction of the intensity by a factor 10 requires an increase in the number of images by a factor of 100. A full list of used exposure times and corresponding doses can be found in table 2.

3. Dynamics of casein micelles obtained by low dose XSVS

3.1. Dynamics of native casein micelle solutions

We first investigate a native casein micelle solution obtained from commercially available skim milk powder. The structure of casein micelles has been investigated extensively with x-ray scattering methods, using different approaches for modeling and interpretation of the data due to the hierarchical structure [32–35]. Dynamics of casein micelles have primarily been studied by light scattering methods and rheology [36]. Due to the strong turbidity of the sample, these measurements were either limited to diluted samples, used advanced cross-correlation schemes to suppress the strong multiple scattering contribution [37], or where restricted to the multiple scattering regime using diffusing wave spectroscopy [38, 39]. In this context, XSVS in the ultra-small angle regime offers the advanced capability of obtaining the full $q$- and direction-dependent information of such concentrated soft matter samples.

The averaged SAXS intensity is displayed in figure 2 (left). No structural changes were found as a function of exposure time and only slight differences were seen for two different batches which were measured at two different instruments, respectively. The SAXS data was modelled by a polydisperse sphere model

$$I(q) \propto \int_0^\infty P(q, R)N(R)V^2(R) \, dR,$$

with the form factor given by equation (1) and the distribution of sizes modelled as a logarithmic normal distribution

$$N(R) = \frac{1}{\sqrt{2\pi}R\sigma} \exp \left( -\frac{(\ln R - \mu)^2}{2\sigma^2} \right).$$

The resulting size distributions are displayed in figure 2 (right). From these, mean radii can be obtained as $R_A = 65$ nm and $R_B = 62$ nm, which is close to values reported in comparable studies ($R \approx 70$ nm) [33]. Additionally, we retrieve the mean radii of the intensity weighted distribution function $(N(R) \propto V^2(R)N(R)$, dashed lines) as $R_A^i = 139$ nm and $R_B^i = 149$ nm.

The measured speckle contrast $\beta(q, \tau)$ for the data set of batch A is displayed in figure 3. We observe a clear dependence of $\beta$ on exposure time $\tau$ and on $q$ with high statistical accuracy, reflecting the dynamical behavior of the sample. For a quantitative evaluation, the data points are fitted following [29]

$$\beta(q, \tau) = \beta_0 \frac{\exp(-2\tau\Gamma(q)) - 1 + 2\tau\Gamma(q)}{2(\tau\Gamma(q))^2},$$

where $\beta_0$ is the initial speckle contrast and $\Gamma(q)$ represents the scattering intensity of the sample. The resulting size distributions are displayed in figure 2 (right). From these, mean radii can be obtained as $R_A = 65$ nm and $R_B = 62$ nm, which is close to values reported in comparable studies ($R \approx 70$ nm) [33]. Additionally, we retrieve the mean radii of the intensity weighted distribution function $(N(R) \propto V^2(R)N(R)$, dashed lines) as $R_A^i = 139$ nm and $R_B^i = 149$ nm.

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Figure 2. (Left) SAXS intensities measured for two different batches of casein micelles. (Right) Size distribution of the casein micelles as obtained from fitting equation (6) to the data in the left panel (solid lines). The dashed lines show the intensity weighted size distributions.

Figure 3. Speckle contrast $\beta(q, \tau)$ for a native casein micelles solution, measured as a function of $q$ and exposure time $\tau$ at beamline ID02 (batch A). Solid lines present fits of equation (8), describing diffusive motion. The inset shows the retrieved relaxation rates $\Gamma(q)$, measured at two different beamlines (batch A and B, respectively). A linear dependence of $\Gamma$ with $q^2$ can be observed, characteristic for simple diffusive motion.

which corresponds to an ISF of a system exhibiting diffusive motion described by an exponential decay

$$|g_1(q, t')| = \exp(-t'\Gamma(q)).$$

Here the relaxation rate $\Gamma(q)$ is given by $\Gamma(q) = D_0q^2$, so that the free diffusion coefficient $D_0$ can be obtained from the linear refinement as shown in the inset of figure 3.

The hydrodynamic radius is given by

$$R_{H1} = \frac{k_B T}{6\pi\eta D_0},$$

with $T$ and $k_B$ being the temperature and the Boltzmann constant, respectively. The viscosity $\eta = 1.5$ cP of skimmed milk was taken from literature [40, 41]. Finally, we obtain $R_{H1} = (149 \pm 14)$ nm (corresponding to the displayed correlation function) and $R_{H1} = (188 \pm 12)$ nm.

In order to compare the results from SAXS and XSVS, two influences on the obtained sizes have to be taken into account. First, casein micelles consist of a stabilizing brush layer ($\approx 11$ nm [33]), which due to its high hydration has only low contrast in SAXS but contributes to the apparent hydrodynamic radius. Therefore, we expect to measure a correspondingly larger hydrodynamic radius from XSVS as compared to the mean radius obtained by SAXS. Second, due to the large polydispersity of casein micelles, the measured hydrodynamic radius by XSVS is the mean radius of the intensity weighted size distribution and should in consequence be compared to $R^l \approx 139–149$ nm. Therefore, we conclude that there is good agreement between both techniques.
3.2. Dynamics upon acidification

Manipulating the structure and stability of casein micelle solutions is well established and essential for applications like cheese or yogurt production [42–45]. For cheese this is in general achieved by enzymatic cutting of the brushed κ-casein surface layer, denoted renneting. The hairy outer layer can also be decharged and ultimately collapsed by lowering the solution pH. This is for example achieved by the use of actio lactobacilli bacteria as in yogurt production.

We create such a denaturated state by changing the solution pH to 4.8 via careful titration with HCl and equilibrating the sample for 48 h. The structural change witnessed by the SAXS curves are displayed in figure 4 (left). Different influences of acidification on the structure and dynamics of casein micelles are reported in literature [46–48]. Due to the reduced pH, the charge on the repulsive stabilizing layer decreases. This lowers the colloidal stability and leads to aggregation of the sample, which can be observed by an upturn at low \(q\) values in the SAXS intensity. Additionally, the decreased pH is known to dissociate the calcium phosphate in the micelles and therefore destabilizing the internal structure. This leads to a reduced globular compactness as evidenced by the reduced peak in the Porod plot (inset, figure 4 left). However, a certain degree of structural integrity of the casein micelles remains, indicated by the preserved \(q^{-4}\) decay of the scattering (corresponding to a plateau in the Porod plot at high \(q\)). As a consequence, certain deviations from purely colloidal gels are expected and observed for acidified casein micelles gels [49].

From an experimental point of view, especially in the broader context of aggregate formation, phase transitions, solidification and gelation, beam damage effects can quickly accumulate due to reduced diffusion and exchange. As a result, such investigations are especially prone to radiation damage effects in sequential measurement schemes. Here, we demonstrate that even completely arrested samples can be measured with XSVS, without signatures of radiation damage effects.

The corresponding \(\beta(q, \tau)\) values are displayed in figure 4 (right). Due to the long equilibration time, we expect the sample to have reached a kinetically arrested state and indeed we find even for the longest exposure times \(\beta(q, \tau) \approx \beta_0\). We consider this an important demonstration of the measurement scheme being completely free of beam damage effects, since any beam induced influence to the sample would blur the speckle pattern with increasing exposure time. Potentially, this would allow to measure out-of-equilibrium conditions in-situ, following simultaneously the structure and dynamics after the pH induced transition.

3.3. Length scale dependent dynamics

An important feature of x-ray based, multi-speckle scattering techniques is the possibility of following structural and \(q\)-dependent dynamical information simultaneously. In concentrated solutions exhibiting strong interparticle interactions, the molecular displacements deviate from a Gaussian distribution, yielding a \(q\)-dependent diffusion coefficient \(D(q)\) dominated by both static correlations and hydrodynamic protein–protein interactions mediated by the solvent [50]. Measurements of \(D(q)\) allow distinguishing the different types of interactions by the short- and long-time diffusion coefficients at varying length scales.

We demonstrate the capability of determining \(D(q)\) with the presented measurement scheme by using a concentrated skim milk solution, which was produced by dissolving three times the amount of skim milk powder as compared to the native sample. The measured SAXS curve is plotted in figure 5 (left), together
with the $I(q)$ of the native sample. The formation of a shoulder at around $q = 3 \times 10^{-2}$ nm$^{-1}$ can be observed, stemming from the increasing direct particle interactions and thus an evolving static structure factor in the scattering intensity.

The corresponding $\beta(q, \tau)$ values are displayed in figure 5 (right). In order to expand the measured decay rates over a wider $q$-range, we additionally include $q$-bins where the lowest exposure times did not provide enough intensity for a reliable contrast determination or where the longest exposure times are not in the sparse scattering regime anymore. Therefore, we set a threshold of $3 \times 10^{-3} < \langle k \rangle < 10$, and exclude data points outside of this range from the plot and the fit.

The data points are fitted following equation (8), and the obtained relaxation rate $\Gamma$ is plotted as a function of $q^2$ in the inset of figure 5 (right). The relaxation rate of the concentrated solution displays clear deviation from the Brownian behavior ($\Gamma^* \propto q^2$, black dashed line). This deviation is additionally depicted in figure 5 (left) as $D_0/D(q)$ (black data points). $D_0/D(q)$ primarily reflects the $q$-dependent static structure factor $S(q)$ following $D(q) = D_0 H(q)/S(q)$, where $D_0$ is the Brownian diffusion coefficient of the diluted solution, modified by the hydrodynamic function $H(q)$, which captures the effect of hydrodynamic interactions [51, 52]. The peak in $D_0/D(q)$ thus resembles the peak in $S(q)/H(q)$ and indeed the positions of the shoulder in the SAXS curve and the peak in $D_0/D(q)$ coincide at $q = 3 \times 10^{-2}$ nm$^{-1}$.

4. Extension of Bio-XSVS to smaller length scales

Having demonstrated that the dynamics of radiation sensitive samples can be measured with low dose XSVS, we now estimate the feasibility of our approach to cover an extended $q$-range corresponding to relevant length scales from several hundreds of nanometer down to a few nanometer. The crucial quantity for such experiments is how much dose $\bar{D}$ is required on the sample in order to collect a sufficiently high intensity $\langle k \rangle$ per pixel and acquisition, while at the same time conserving the speckle contrast $\beta_0$. The quantity $\bar{D}/\langle k \rangle$ can therefore be understood as a relative cost merit, which should be minimized in order to optimize the experimental conditions.

In a first approach, we assume that with the same USAXS setups (e.g. beamline P10, PETRA III: sample-detector-distance $L = 20$ m, photon energy $E = 8$ keV, beam spot size $a = 60 \mu$m, Si-111 monochromator, EIGER detector) we can cover all required $q$-values. This approach can only serve as a lower limit estimation, as it already neglects geometrical limitations such as finite detector sizes or the restriction to a forward scattering geometry. Still, we can estimate the theoretical $\bar{D}/\langle k \rangle$ ratio at $q$-values corresponding to intermolecular distances for each protein ($q = 2\pi/(4 \cdot R_G)$), using reported values for the radius of gyration $R_G$ and the absolute scattering intensity of each protein [53] (red data points). Details of the calculation were reported in [2]. All the data points follow approximately a $q^2$ behavior, provided as a guide to the eye (red dashed line in figure 6). Additionally, we include the measured $\bar{D}/\langle k \rangle$ values of the previously discussed casein micelles solutions (for the largest and smallest $q$-values measured at both beamlines respectively (cyan and magenta data points in figure 6)).

6 In practice the required $q$-values could be reached also by a reduction of the sample-detector-distance, which would however require in consequence a smaller x-ray focus and therefore leading to a larger $\bar{D}/\langle k \rangle$. 

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**Figure 5.** XSVS from a concentrated skim milk sample, obtained at beamline ID02. (Left) SAXS intensities measured from the native (red) and the concentrated sample (blue). Black points: $D_0/D(q)$ with $D(q)$ denoting the $q$-dependent diffusion coefficient. Color shaded regions depict the $q$-ranges for which the speckle contrast was analyzed. (Right) Speckle contrast $\beta$ of concentrated skim milk sample as a function of $q$-bins and exposure time. The symbol colors follow the $q$-bins (left). The solid lines display fits of equation (8) to the data. The inset shows the relaxation rates $\Gamma(q^2)$, with a linear fit depicted as black dashed line.
Figure 6. Comparison of different experimental setups in terms of deposited dose on the sample per mean pixel intensity \( \langle k \rangle \). Measured values for casein micelles at beamline P10 (PETRA III) and ID02 (ESRF prior to the ESRF-EBS upgrade) (cyan and magenta data points). Red data points are estimated values at \( q/4 \) where \( q = 2\pi/R \), from measured absolute scattering intensities of different proteins [53], calculated with the same experimental parameter as used in this experiment at beamline P10. Green data points correspond to estimations using a proposed beamline design for biological coherent scattering applications (sample-detector-distance \( L = 25 \) m, photon energy \( E = 16 \) keV, beam spot size \( a = 50 \) μm, Si-311 monochromator) as well as the improved source properties expected for the upgraded PETRA IV storage ring.

Considering a maximum tolerable dose of \( \tilde{D} = 100 \) Gy and a minimum scattering intensity of \( \langle k \rangle = 10^{-2} \), we estimate the criterion of \( \tilde{D}/\langle k \rangle \leq 10^4 \) Gy for successful Bio-XSVS experiments. It can be seen that many of the displayed proteins exceed this value. Additionally, the speckle contrast at these larger \( q \)-values is also considerably reduced, as displayed by the red solid line in the inset of figure 6. Therefore, we conclude that a simple extension of the experimental scheme to smaller length scales is not possible without revisiting the experimental setup.

The new generation of diffraction limited storage rings (DLSRs) such as the recently inaugurated ESRF-EBS [7] or the planned PETRA IV facility [5, 6, 9] provide x-ray beams with a higher coherent fraction, larger coherence length and higher coherent flux, especially at higher photon energies. As the presented measurements were performed before the upgrade of the ESRF storage ring, we expect that already now measurements on casein micelles can be expanded considerably to shorter time scales at the ID02 beamline [54], since due to the increased coherent flux (> \( 10^{12} \) ph s \(^{-1} \)) a speckle pattern with the same intensity can be obtained within a shorter acquisition time. The investigation of smaller, monomeric proteins would however still be very challenging, as the ratio of \( \tilde{D}/\langle k \rangle \) is independent of the coherent flux and at ID02 the experimental geometry is restricted to forward scattering [54] and the speckle contrast decreases sharply for higher \( q \) values [25].

The improved coherent properties of x-ray radiation provided by new DLSR sources also open up new possibilities for designing low-dose coherent scattering experiments, with the aim of spreading the absorbed x-ray energy over a larger sample volume. In a nutshell, the larger transversal coherence length allows to increase the x-ray spot size on the sample while conserving the speckle contrast. Due to the higher incident coherent flux, the longitudinal coherence length can be increased by using a Si-311 monochromator while keeping a sufficient coherent flux on the sample. This, in combination with a higher photon energy, allows to increase the sample thickness. A more detailed discussion on the optimization of the scattering setup can be found in [2].

The envisioned increase in sampled volume also requires a high resolution scattering geometry to resolve the consequently smaller speckle on the detector and at the same time cover the targeted \( q \)-range. For this purpose, we propose a new beamline design optimized for biological coherent scattering applications, featuring a 25 m long, rotatable (horizontal 2Θ) detector arm. We repeat the previous calculations with this proposed setup (sample-detector-distance \( L = 25 \) m, photon energy \( E = 16 \) keV, beam spot size \( a = 50 \) μm, Si-311 monochromator) and using the predicted source properties of PETRA IV [9]. The corresponding data points are plotted in green in figure 6. One can observe that a decrease of the
deposited dose per $\langle k \rangle$ by about a factor 15 can be achieved, while even increasing the speckle contrast at larger $q$-values (inset). With this, biological samples can be studied on the full $q$-range of relevance, keeping the deposited dose per scattered photon below the threshold of $D/\langle k \rangle \leq 10^4$ Gy for all considered cases.

5. Conclusion

We demonstrate that dynamical information on biological, protein based samples in solution can be obtained from low dose XSVS measurements, with deposited doses per acquisition well below critical dose limits. It was shown that simple Brownian diffusion can be characterized for a native suspension of casein micelles, and the retrieved dynamical information matches well with expectations based on structural information that was obtained simultaneously by SAXS. In the case of a static soft matter system, no dynamics induced by radiation damage was observed, confirming the possibilities of XSVS for radiation sensitive systems. Additionally, more complex solution environments can be studied, such that for instance diffusive dynamics characterized by $D(q)$ in a crowded solution can be accessed experimentally.

We additionally show that XSVS is an especially well suited technique in combination with new generation x-ray sources. Maybe counter-intuitively, the increased coherent flux in combination with an increased coherence length, increased photon energy as well as dedicated instrumention can be used to reduce the dose on the sample per scattered photon $D/\langle k \rangle$ and enable the investigation of small, monomeric proteins. It should be emphasized that the increase in coherent flux by novel x-ray sources can be fully utilized by this technique, also for the dynamics investigations of biological, radiation sensitive samples. The fastest accessible time scales are not limited by the acquisition rate of the detector, but only by the strength of the signal and the ability to determine the speckle contrast of low intensity speckle patterns with high statistical accuracy. Instruments for coherent scattering using faster detectors [25, 55, 56] and high repetition rate sources such as European XFEL [57, 58] will make it possible to obtain large sets of data in shorter time, in order to gather the required statistics and standardize the presented measurement scheme. In this sense, also the development of multi mega pixel detectors with higher sensitivity for single photon detection will push the detection limit for accurate speckle contrast determination towards lower count rates, enabling faster timescales to be probed and reducing the dose on the sample even further. Therefore, XSVS in combination with new coherent x-ray sources and single photon sensitive detectors will make the dynamical investigation of smaller, faster, and more radiation sensitive biological samples feasible.

Data availability statement

The data that support the findings of this study are available upon reasonable request from the authors.

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