Wolf-Rayet and LBV Nebulae as the Result of Variable and Non-Spherical Stellar Winds

Mordecai-Mark Mac Low

Max-Planck-Institut für Astronomie, Königstuhl 17, D-69117 Heidelberg, Germany

Abstract. The physical basis for interpreting observations of nebular morphology around massive stars in terms of the evolution of the central stars is reviewed, and examples are discussed, including NGC 6888, OMC-1, and η Carinae.

1 Introduction

The nebulae observed around massive, post-main sequence stars appear to consist of material ejected by the central stars during earlier phases of their evolution, rather than ambient interstellar matter. Models of these nebulae can be used to constrain the mass-loss history of the stars, giving an important input for stellar evolution models. Understanding the structure of these nebulae also clarifies the initial conditions for the resulting supernova remnants, which will interact with the circumstellar material for most of their observable lifetimes before encountering the surrounding interstellar medium.

A strong stellar wind sweeps the surrounding interstellar gas into a stellar wind bubble as shown in Figure 1. The stellar wind expands freely until it reaches a termination shock. If this shock is adiabatic, the hot gas sweeps up the surrounding ISM into a dense shell, forming a pressure-driven or energy-conserving bubble that sweeps up the surrounding ISM into a dense shell growing as \( R \propto t^{3/5} \) in a uniform medium (Castor, McCray, & Weaver 1975). Should the termination shock be strongly radiative due to high densities or low velocities in the wind, the bubble only conserves momentum and will grow as \( R \propto t^{1/2} \) (Steigman, Strittmatter, & Williams 1975). For more general discussions of blast waves in non-uniform media, see Ostriker & McKee (1988), and Bisnovatyi-Kogan & Silich (1995), as well as Koo & McKee (1990).

When these stars leave the main sequence, they pass through phases of greatly increased mass loss. These slow, dense winds expand into the rarefied interior of the main sequence bubble until their ram pressure \( \rho_w v_w^2 \) drops below the pressure of the bubble. (Should the main sequence bubble have cooled relatively quickly, this may never occur.) As the mass loss rate and velocity of the central wind vary during the post-main sequence evolution of the central star, these denser winds can in turn be swept up, producing the observed ring nebulae around evolved massive stars.

During their evolution, these nebulae are subject to a number of hydrodynamical instabilities, as well as thermal instabilities (e. g. Strickland & Blondin 1995). I explain how understanding the physical basis of the hydrodynamical
instabilities gives insight into the dynamics of observed nebulae. High-resolution observations of nebular morphology can thus be used to constrain the mass-loss history of the central star.

I then describe how typical stellar evolutionary scenarios can generate observed nebular morphologies, and show semi-analytic and numerical models derived from these scenarios. For example, a star with a stellar wind varying from fast to slow and back again will have a clumpy circumstellar nebula due to hydrodynamical instabilities in the shell (García-Segura, Langer & Mac Low 1996). Nonspherical winds and stellar motion can add to the morphological richness of the resulting nebulae, as in the nebula around \( \eta \) Car (Langer, García-Segura, & Mac Low 1998). A recent review of this topic is Frank (1998).

2 Shell Instabilities

Gas swept up by a stellar wind will usually be subject to different instabilities. An adiabatic, decelerating shell with a density contrast across the shock of less than 10 in a uniform medium is stable. However, relaxing any of these constraints will lead to instabilities as I now describe.

2.1 Rayleigh-Taylor Instability

If the swept-up shell is denser than the stellar wind, as will be true in virtually all cases where a shell exists at all, the shell will be subject to RT instabilities if the contact discontinuity between the shocked stellar wind and the shell accelerates. This can be due to an external density gradient steeper than \( r^{-2} \) or to a sufficiently fast increase in the power of the central stellar wind, though these two mechanisms will lead to different shell morphologies, as I discuss below.

The RT instability occurs when the effective gravity due to acceleration points from a denser to a more rarefied gas. We can understand its driving mechanism by considering how the potential energy will change if we interchange a parcel of dense gas having mass \( m_1 \) with a parcel of more rarefied gas having \( m_0 < m_1 \), as shown in Figure 2. The potential energy before the interchange
is given by $E_i = m_1 gz + m_0 g(z - \Delta z)$ which is greater than the potential energy after the interchange $E_f = m_0 gz + m_1 g(z - \Delta z)$ due to the difference in the masses. The decrease in potential energy drives an exponentially growing interchange of the two fluids.

When a RT instability occurs due to an external density gradient, dense fragments of shell are left behind as the less dense interior expands out beyond them, creating the characteristic bubble and spike morphology seen, for example, in models of superbubble blowout (e. g. Mac Low, McCray, & Norman 1989). The Wolf-Rayet ring nebula NGC 6888 shown in Figure 3 provides another example. Here a fast, rarefied Wolf-Rayet wind has swept up the slow, dense red supergiant wind that preceded it. While it was still sweeping up the slow wind, it was marginally stable to RT instabilities. However, at the outer edge of the slow wind, the sharp density gradient triggers RT instabilities, as modelled by García-Segura & Mac Low (1995) with the astrophysical gas dynamics and magnetohydrodynamics code ZEUS\(^1\) (Stone & Norman 1992).

On the other hand, when a RT instability occurs due to an increase in power of the driving wind, some of the dense fragments of shell actually get shot out ahead of the bulk of the fragmenting shell, producing a markedly different morphology (Stone, Xu, & Mundy 1995). Although these fragments represent only a small fraction of the total mass of the shell, they can produce a very striking set of bow shocks in their wake. An example of this occurring around one or more pre-main sequence stars is given by the “bullets” observed around OMC-1 (Lane 1989, Allen & Burton 1993) in the Orion star forming region, as confirmed by McCaughrean & Mac Low (1997).

### 2.2 Vishniac Instability

If a pressure-driven shell is decelerating, but thin, with a density contrast across the shock of at least 25 for a stellar-wind bubble expanding into a uniform medium (Ryu & Vishniac 1988), or 10 for a point explosion (Ryu & Vishniac 1987), it will be subject to the Vishniac overstability (Vishniac 1983). This has been confirmed experimentally using blast waves generated by high-powered lasers propagating into gases with low and high adiabatic indexes (Grun et al. 1991).

\(^1\) Available by registration with the Laboratory for Computational Astrophysics at lca@ncsa.uiuc.edu
Fig. 3. Comparison between morphology of NGC 6888 in O[iii] (in an image taken by K. B. Kwitter with the Burrell-Schmidt telescope of the Warner and Swasey Observatory, Case Western Reserve University), and a numerical simulation of RT instability due to a fast wind sweeping over the end of a slow, dense wind (García-Segura & Mac Low 1995). The model image shows a cross-section of the density structure in grayscale with black indicating high density and white low density.

The mechanism of the Vishniac overstability can be understood by considering a thin, decelerating shell driven from within by a high-pressure region, as shown in Figure 4. From within it is confined by thermal pressure acting normal to the shell surface, as adjacent regions can communicate with each other by sound waves, while from outside it is confined by ram pressure acting parallel to the velocity of propagation, as the shell moves supersonically into the surrounding gas. In equilibrium, these two forces remain in balance. Should the shell be perturbed, however, the thermal pressure will continue to act normally, but the ram pressure will now act obliquely, giving a transverse resultant force that drives material from “peaks” into “valleys” of the shell. The denser valleys will be decelerated less than the rarefied peaks, however, so that the positions of peaks and valleys are interchanged after some time. Vishniac (1983) showed that this overstable oscillation can grow as fast as $t^{1/2}$. It saturates when the transverse flows in the shell become supersonic and form transverse shocks, so that the end result of Vishniac instability is a shell with transonic turbulence and moderate perturbations (Mac Low & Norman 1993).

2.3 Nonlinear Thin Shell Instability

Should the driving wind cool immediately behind its termination shock, for example because of exceptionally high mass-loss rates, it can form a decelerating shell that is momentum-driven rather than pressure-driven, so that it is effectively confined on both sides by ram pressure from shocks. Such a shell is
not subject to the Vishniac instability, and is, in fact, linearly stable. However Vishniac (1994) has shown that if the shell is strongly perturbed, it will still be subject to a nonlinear thin shell instability (NTSI). When the shocks are oblique enough to the direction of flow, they will bend the streamlines passing through them, so that mass is driven towards the extrema of the perturbation. Numerical simulations by Blondin & Marks (1996), using a piecewise parabolic hydrocode called VH-1, have shown that the end result is a catastrophic breakup of the shell into a turbulent layer that grows in time.

3 A Final Example: Eta Carinae

As an example of how knowledge of these different instabilities can be used to constrain the evolution of a star, consider the example of the Homunculus Nebula around η Car. Langer, García-Segura, & Mac Low (1998) computed several two-dimensional models of it using ZEUS, following a basic scenario in which a luminous blue star with a fast stellar wind undergoes an outburst during which it has a much slower and denser wind strongly shaped by rotation, as described by Bjorkman & Cassinelli (1993), but then reverts to its previous state with a fast, rarefied wind. They chose two different values for the post-outburst wind, one consistent with current observed values of $\dot{M} = 1.3 \times 10^{-3} M_\odot \, \text{yr}^{-1}$ and $v_w = 1300 \, \text{km s}^{-1}$, and one with a faster, lower mass loss wind having $\dot{M} = 1.7 \times 10^{-4} M_\odot \, \text{yr}^{-1}$ and $v_w = 1800 \, \text{km s}^{-1}$. As shown in Figure 5, the slower, denser wind cools upon shocking, forming a momentum-driven shell that fragments due to the NTSI, producing a sharp, spiky shell morphology. On the other hand, the faster wind does not cool completely, and forms a bubble subject to Vishniac instabilities, giving it a much more curved, cauliflower-like appearance. Comparison to the high-resolution observations (Humphreys & Davidson 1994; Morse, Davidson, & Ebbets 1997) reveals that the actual morphology strongly resembles a three-dimensional version of the model with the faster wind. Langer et al. (1998) suggest that this reflects the typical behavior of the wind over the century since the outburst, and that the current wind properties are actually exceptional, and perhaps even indicative of another outburst on its way.
Fig. 5. Two-dimensional density distributions from models of η Car by Langer, García-Segura, & Mac Low (1998) with faster and slower post-outburst wind showing Vishniac instabilities and the NTSI respectively. Note how the faster wind model resembles a cross-section through the cauliflower-like observed lobes.

This suggestion is supported by the gradual brightening of η Car over the last decades (Humphreys & Davidson 1994).

This work has made use of the NASA Astrophysical Data System Abstract Service. I thank the organizers for their invitation and their support of my attendance at this meeting.

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