Probing transfer to unbound states of the ejectile with weakly bound $^7\text{Li}$ on $^{93}\text{Nb}$

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The two-step process of transfer followed by breakup is explored by measuring a rather complete set of exclusive data for reaction channels populating states in the ejectile continua of the $^7\text{Li}+^{93}\text{Nb}$ system at energies close to the Coulomb barrier. The cross sections for $\alpha + \alpha$ events from one proton pickup were found to be smaller than those for $\alpha + d$ events from one neutron stripping and $\alpha + t$ events from direct breakup of $^7\text{Li}$. Coupled channels Born approximation and continuum discretized coupled channels calculations describe the data well and support the conclusion that the $\alpha + d$ and $\alpha + \alpha$ events are produced by direct transfer to unbound states of the ejectile.

Exploring the properties of weakly-bound stable/unstable nuclei via transfer reactions is a topic of current interest and also a focus of the next generation of high-intensity isotope-separator on-line (ISOL) radioactive ion beam facilities. Due to the low breakup threshold of such nuclei, population of the continuum is probable and consequently a large coupling effect is expected at energies around the Coulomb barrier. This may take place directly through inelastic excitation of the projectile (prompt or resonant breakup) or by neutron transfer leaving the ejectile in an unbound state (transfer-breakup) [4][14]. The large positive Q-values for the transfer of neutrons from light neutron-rich projectiles to heavy targets also emphasize the role of neutron evaporation following transfer [10][17]. Exclusive measurements are essential to disentangle these reaction channels. Also, complete measurements of different reaction channels as well as theoretical calculations are required to understand the interplay between them. Among the limited exclusive measurements aimed at studying different breakup processes, very few data on absolute cross sections are available for direct breakup [12][13][15], while for transfer-breakup absolute differential cross sections are only available for the neutron transfer channels at energies close to the Coulomb barrier [5][7].

Among the processes discussed above, investigation of the two-step reaction mechanism, viz., one nucleon transfer followed by breakup, is of current interest for the weakly-bound stable nuclei $^6,7\text{Li}$ and $^9\text{Be}$ [5][9][12][14][15]. This complex process needs the simultaneous understanding of both the breakup and transfer reactions. In an earlier measurement of the $^7\text{Li}+^{48}\text{Cu}$ system [5] it was observed that 1n-stripping leading to $^6\text{Li}$ in its unbound $3^+$ excited state is more probable than inelastic excitation of $^7\text{Li}$ to its resonant states. Recent measurements with $^7\text{Li}$ [9][10], the importance of 1p-pickup over the direct breakup of the projectile was highlighted while explaining the suppression of fusion at energies above the Coulomb barrier. Hence, understanding the mechanism of projectile breakup—whether direct or transfer breakup—is crucial while studying the reaction dynamics of weakly bound nuclei.

This communication reports the first simultaneous measurement of absolute differential cross sections for both 1p-pickup and 1n-stripping followed by breakup of the ejectile as well as direct breakup of the weakly bound projectile over a wide angular range. A simulation code has been developed using the Monte Carlo technique to interpret the observables of different breakup processes and estimate the efficiency for coincident detection of the breakup fragments. Angular distributions for elastic scattering and nucleon transfer to bound states have also been measured. Coupled channels Born approximation (CCBA) and continuum discretized coupled channels (CDCC) calculations which explain the large number of observables are presented.

The experiment was carried out at the Pelletron-Linac facility, Mumbai, with $^7\text{Li}$ beams of 24, 28 and 30 MeV. A self-supporting $^{93}\text{Nb}$ foil of thickness $\sim 1.75$ mg/cm$^2$ was used as a target. The requirements of high granularity to detect low-lying resonant states and large solid angle to measure low cross section events were achieved using segmented large area Si-telescopes of active area $5 \times 5$ cm$^2$. The $\Delta E$ detector (50 $\mu$m thick) was single-sided and the E detector (1.5 mm thick) was double-sided with 16 strips allowing a maximum of 256 pixels. Two such telescopes, set 30° apart, were mounted at a distance of 16 cm from the target on a movable arm in a scattering chamber. In this geometry, the cone angle between the two detected fragments ranged from 1° to 24°. The angular range 30°–130° (around the grazing angle) was covered by measurements at different angle settings. Three Si surface-barrier detector telescopes (thicknesses: $\Delta E \sim 20-50$ $\mu$m, $E \sim 450-1000$ $\mu$m) were used to obtain the elastic scattering angular distribution at forward an-
The excitation energy of the target-like nuclei was determined using the missing energy technique. For the transfer reactions, this was found to peak around the energy $E^* = Q_{\text{gs}} - Q_{\text{opt}}$, as expected from semi-classical theory [20]. Here $Q_{\text{gs}}$ and $Q_{\text{opt}}$ are the ground state and optimum Q-values, respectively. For 1p-pickup $E^* (^{92}\text{Zr})$ peaks at ~3 MeV and for 1n-stripping $E^* (^{94}\text{Nb})$ peaks at ~0.5 MeV. The data presented in Fig. 1 (a) and (b); (c) and (d); (e) and (f) correspond to excitation energies $E^* (^{92}\text{Zr})$ up to 5 MeV, $E^* (^{94}\text{Nb})$ up to 1 MeV and $E^* (^{94}\text{Nb})$ up to 2 MeV, respectively.

The efficiency for the detection of fragments in coincidence was estimated using the Monte Carlo technique taking into account the excitation of the target as well as the ejectile, the Q-value of the reaction, the energy resolution and detection threshold. The efficiency depends on the velocity of the ejectile prior to breakup as well as the relative velocity of the fragments [21]. The scattering angle of the ejectile prior to breakup was assumed to be isotropic. The scattered energy of the ejectile was calculated using kinematics. The breakup fragment emission in the rest frame of the ejectile was also considered to be isotropic. The velocities of each fragment in the rest frame of the ejectile were calculated using energy and momentum conservation laws. These velocities were added to the velocity of the ejectile prior to breakup to get their velocities in the laboratory frame. It was checked whether both fragments hit two different vertical and horizontal strips. Events satisfying this condition were considered as detectable events for estimation of the efficiency. The conversion of the energy and scattering angle from the laboratory frame to the c.m. frame of the target-projectile in event-by-event mode automatically takes care of the Jacobian of the transformation.

The simulated kinetic energy spectra of the α particles resulting from different breakup processes are shown
in Fig. 1. The relative energy distributions for $\alpha-\alpha$, $\alpha-d$ and $\alpha-t$ breakup were assumed to be Gaussian, centered at 92, 710 and 2160 keV, respectively. While the yields corresponding to the high and low energy $\alpha$ particle are symmetric for $\alpha-\alpha$ breakup, they are found to be asymmetric for $\alpha-d$ breakup. Such an asymmetry was also observed in Ref. 7 and different cross sections for the high and low energy $\alpha$ particles were obtained. The asymmetry is found to arise from kinematic focusing, which depends on the fragment mass asymmetry, relative energy, relative angle and the scattering angle of the ejectile.

The angular distributions of elastic scattering, projectile breakup and transfer followed by breakup for the $^7\text{Li}+^93\text{Nb}$ system at 28 MeV are shown in Fig. 2. The elastic scattering data are presented in Fig. 2 (a). The errors on the data points are due to statistics. The $^7\text{Li}^* \rightarrow \alpha+t$ breakup via the $7/2^-$ state and the continuum below this resonance are shown in Fig. 2 (b). The cross sections for 1p-pickup leading to the $^8\text{Be}(g.s.)$ are shown in Fig. 2 (c). These data are restricted to $^{92}\text{Zr}$ excitation energies up to 3.0 MeV, as information on the spectroscopic factors is available only in this energy range. For 1n-stripping, the cross sections for $\alpha+d$ breakup events from the $^6\text{Li}$ $3_1^+$ (2.18 MeV) state are shown in Fig. 2 (c). Excited states of $^{94}\text{Nb}$ up to 1.0 MeV were considered.

The differential cross sections for $\alpha+d$ events from the breakup of $^6\text{Li}$ formed after 1n-stripping are larger than those for $\alpha+t$ events from the resonant breakup of $^7\text{Li}$, while those for $\alpha+\alpha$ events due to 1p-pickup forming $^8\text{Be}$ are smaller. Integrated cross sections obtained assuming a Gaussian shape are listed in Table 1. The total exclusive cross sections for $\alpha$ production form a small fraction of the inclusive cross section (inset Fig. 2 (a)), indicating that the main $\alpha$ production mechanism is due to other processes, most likely fusion-evaporation and $t$-stripping/capture. Similar to those described in Refs. 20 and 21, statistical model calculations using the code PACE-23 put the fusion-evaporation contribution to the total $\alpha$ yield at between 10% ($E_{\text{beam}} = 24$ MeV) to 20% ($E_{\text{beam}} = 30$ MeV).

Cross sections for 1n-stripping ($Q_{\text{sp}} = -20$ keV) populating the $^6\text{Li}(3_1^+)$ resonance and 1p-pickup ($Q_{\text{sp}} = 11.21$ MeV) populating $^8\text{Be}(g.s.)$ at 24, 28 and 30 MeV are compared in Fig. 3 and Table 1. The angular distributions for both reactions are bell shaped with peaks at the respective grazing angles for the different beam energies. The cross sections for 1p-pickup (with a large positive $Q_{\text{sp}}$) are found to be smaller than those for 1n-stripping at all energies, which may be attributed to poor kinematic matching. The $\alpha+t$ events from the $^7\text{Li}(7/2^-)$ state could not be detected at 24 and 30 MeV due to the detection threshold. Cross sections for 1n-stripping populating $^6\text{Li}$ in its ground state and $^{94}\text{Nb}$ ($E^* \leq 1$ MeV) were obtained independently from the inclusive data and are listed in Table 1.

Two sets of calculations were performed to analyze the data. Calculations for elastic scattering and direct breakup were carried out within the CDCC formalism using the cluster folding model of $^7\text{Li}$. The CCBA formalism was employed for transfer-breakup processes, using potentials that describe the elastic scattering data. The code Fresco was used in all cases. The $^7\text{Li} \rightarrow \alpha+t$ breakup data at 28 MeV were analyzed with CDCC calculations, similar to those described in Ref. 25 except that the continuum bins were of width $\Delta k = 0.1$ fm$^{-1}$ with $k_{\text{max}} = 0.8$ fm$^{-1}$ and $\alpha+t$ relative angular momenta of $L = 0–4$ and couplings up to multipolarity $\lambda = 4$ were included. The $\alpha+^{93}\text{Nb}$ and $t+^{93}\text{Nb}$ optical potentials required as input to the Watanabe-type folding potentials were taken from the global parameterizations of Refs. 21 and 27, respectively. To obtain...
the best fit to the elastic scattering data the real and imaginary depths of these potentials were renormalized by factors of 0.6 and 0.8, respectively. The results are compared to the elastic scattering and breakup data in Fig. 2 (a) and (b), respectively.

![Graph](image_url)

**FIG. 3.** (Color online) In-stripping and 1p-pickup cross sections for the $^7$Li+$^{93}$Nb system at 24, 28 and 30 MeV. (a) The $\alpha + d$ cross sections for the $(^7$Li,$^6$Li$^*$) reaction. (b) The $\alpha + \alpha$ cross sections for the $(^7$Li,$^8$Be$^*$) reaction. In both panels the dotted, solid and dashed lines correspond to the CCBA calculations at 24, 28 and 30 MeV, respectively.

The $\alpha + d$ coincidence data were analyzed with CCBA calculations of the $^{93}$Nb$(^7$Li,$^6$Li$^*$) $^{94}$Nb in-stripping reaction. In addition to the transfer couplings inelastic excitations of the $^7$Li(1/2$^-$) and the $^6$Li(3$^+_1$) excited states were included in the entrance and exit partitions, respectively. The entrance channel optical potentials were based on the global $^7$Li parameters of Ref. [28] with real and imaginary depths readjusted to fit the elastic scattering data after the inclusion of the $^7$Li couplings. The 3/2$^-$ (g.s.) and 1/2$^-$ (0.478 MeV) states of $^7$Li were treated as members of a K = 1/2 rotational band. The $B(E2; 3/2^- \rightarrow 1/2^-)$ was taken from Ref. [29] and the nuclear deformation length $\delta_2 = 2.4$ fm obtained by fitting the inelastic scattering data of Ref. [30]. The $^9$Li $B(E2; 2^- \rightarrow 1^-)$ was taken from Ref. [31] and the nuclear deformation length $\delta_2 = 1.9$ fm obtained by fitting the sequential breakup data of Ref. [32]. The $^6$Li 1$^+_1$ and 3$^+_1$ states were assumed to be members of a K = 1 rotational band, with the exception that reorientation of the 1$^+_1$ ground state was omitted due to the very small quadrupole moment of this state. The exit channel optical potentials employed the $^6$Li global parameters of Ref. [28] with real and imaginary well depths adjusted to recover the same elastic scattering angular distributions at the appropriate energies when the $^6$Li excitations were included. Spectroscopic factors for the $(^7$Li$^9$Li + n) and $(^9$Nb)$^{93}$Nb + n overlaps were taken from Refs. [33] and [34], respectively. Transfers between the $^7$Li 3/2$^-$ ground state and the $^6$Li 1$^+_1$ and 3$^+_1$ states, the $^7$Li 1/2$^-$ state and the $^6$Li 1$^+_1$ state, plus a total of eight states in $^{94}$Nb (the most strongly populated according to Ref. [34]) were included. The results are compared to the data in Figs. 2 (c) and 3 (a).

Similar CCBA calculations were performed for the $\alpha + \alpha$ coincidence data considering the $^{93}$Nb$(^7$Li, $^8$Be)$^{92}$Zr 1p-pickup process. Entrance channel potentials were as described above. Exit channel optical potentials used $^7$Li global parameters [28] since no $^8$Be potentials are available. Pickup to the 0.0 MeV 0$^+$ resonance of $^8$Be and the 0$^+$ (g.s.), 5$^-$ (2.45 MeV) and 4$^-$ (2.74 MeV) states of $^{92}$Zr were included. The spectroscopic factor for the $(^8$Be$^7$Li$^1$ + p) overlap was taken from Ref. [33] and those for the $(^9$Nb)$^{92}$Zr + p overlaps were obtained by fitting the $^{93}$Nb(d,$^3$He) data of Ref. [35], yielding values of C$^2$S = 1.4, 1.0 and 1.0 for the 0$^+$, 5$^-$ and 4$^-$ states, respectively (N.B. the value of 10.8 in Ref. [35] for the 0$^+$ state appears to be an error, since it is inconsistent with the data plotted on their Fig. 8). The results are compared to the data in Figs. 2 (c) and 3 (b).

We now discuss the current investigation in the context of recent work in this area. A study of the quasielastic excitation function and barrier distribution of the $^7$Li+$^{114}$Sn system found the role played by neu-

### TABLE I. Cross sections for various channels in the $^7$Li+$^{95}$Zr system; $\sigma_{cal}$ denotes the results of CDCC $(^7$Li $(^7$Li + p)$\rightarrow \alpha + t$) and CCBA (other reactions) calculations, see text.

| Channel | $\sigma_{exp}$ (mb) | $\sigma_{cal}$ (mb) |
|---------|---------------------|---------------------|
| $E_{cal}$ = 24 MeV |                      |                     |
| $\alpha$-inclusive | 273 ± 40 | 0.36 |
| $^8$Be(g.s.)$^7$Li $\rightarrow \alpha + \alpha$ | 0.5 ± 0.1 | 0.36 |
| $^8$Be(g.s.$^7$Li $\rightarrow \alpha + \alpha$ | 1.0 ± 0.2 | 0.36 |
| $^6$Li(3$^+_1$) $\rightarrow \alpha + d$ | 5.2 ± 0.5 | 5.5 |
| $^6$Li(g.s.) | 9.9 ± 1.0 | 9.8 |
| $\sigma$-reaction | 1121 |                     |
| $E_{cal}$ = 28 MeV |                      |                     |
| $\alpha$-inclusive | 321 ± 48 | 0.56 |
| $^8$Be(g.s.$^7$Li $\rightarrow \alpha + \alpha$ | 0.7 ± 0.1 | 0.56 |
| $^8$Be(g.s.$^7$Li $\rightarrow \alpha + \alpha$ | 1.3 ± 0.2 | 0.56 |
| $^6$Li(3$^+_1$) $\rightarrow \alpha + d$ | 5.8 ± 0.4 | 6.2 |
| $^6$Li(g.s.) | 11.0 ± 1.2 | 10.9 |
| $^7$Li(7/2$^-$) $\rightarrow \alpha + t$ | 3.3 ± 0.6 | 2.9 |
| $\sigma$-reaction | 1310 |                     |
| $E_{cal}$ = 30 MeV |                      |                     |
| $\alpha$-inclusive | 340 ± 52 | 0.36 |
| $^8$Be(g.s.$^7$Li $\rightarrow \alpha + \alpha$ | 0.6 ± 0.1 | 0.36 |
| $^8$Be(g.s.$^7$Li $\rightarrow \alpha + \alpha$ | 1.5 ± 0.2 | 0.36 |
| $^6$Li(3$^+_1$) $\rightarrow \alpha + d$ | 6.2 ± 0.4 | 6.2 |
| $^6$Li(g.s.) | 11.2 ± 1.5 | 10.3 |
| $\sigma$-reaction | 1489 |                     |

a $E^*$($^{95}$Zr)$\leq 3$ MeV
b $E^*$($^{95}$Zr)$\leq 5$ MeV
tron transfer followed by breakup in the reaction mechanism to be important as a two-step process [18]. An investigation of the 1p-pickup reaction using the classical dynamical model [20] has recently been reported for the 6Li+58Ni system and further measurements were suggested fully to understand the influence of breakup processes—both direct and transfer induced—on fusion [10]. In the present work we have measured absolute cross sections for all major reaction channels leading to breakup processes for a single system, 7Li+58Nb. The rather complete nature of the data set, including elastic scattering, combined with the calculations presented here, enables us to make the following conclusions about both the mechanism and the relative importance of these processes.

The CCBA calculations agree well with the α+d and α+α coincidence data, both in terms of the shapes of the angular distributions and the absolute cross sections (see Table 1 and Fig. 2). Population of the 6Li ground state is also reproduced by the same calculations. Calculations omitting direct population of the 6Li ground state confirmed that transfer to the 6Li 1+ state followed by excitation of the 3+ 1α state makes a negligible contribution, in agreement with Ref. [5]. Taken together, the data and calculations show unequivocally that the mechanism producing the α+d coincidences is direct 1n-stripping to the unbound 6Li 3+ state and the origin of the α+α coincidences is 1p-pickup to 8Be(g.s.). As seen from Table I, the cross sections of 1n-stripping account for ∼2% and 1p-pickup only ∼0.8% (recall that each 8Be contributes two α particles to the total yield) of the inclusive α yields.

The α+t coincidence data are reproduced well by the CDCC calculations. The calculated total 7Li* → α+t breakup cross section (16.8 mb) accounts for ∼5% of the inclusive α yield at Ebeam = 28 MeV, almost twice the combined contribution of 1n-stripping and 1p-pickup.

Overall, the combination of measurements and calculations suggests that at most only ∼8% of the inclusive α yield can be accounted for by these processes. Thus, even allowing for population of the 6Li and 8Be non-resonant continua and the broad 8Be 2+ resonance the main α-particle production mechanism must be due to other sources, most likely fusion-evaporation and t-stripping/capture [2, 4, 5, 19, 22].

In summary, the present work reports for the first time a detailed study of the various breakup mechanisms—1p-pickup and 1n-stripping to unbound states of the ejectile and direct breakup—for the same system at energies close to the Coulomb barrier. CDCC and CCBA calculations were performed to analyze a comprehensive data set comprising elastic scattering, direct breakup and transfer-breakup. These calculations confirmed that the α+d and α+α coincidences mostly result from direct 1n-stripping to the 6Li 3+ state and 1p-pickup to the 8Be 0+ , respectively. The present result also established that the main α production mechanism must be due to other processes, presumably fusion-evaporation and t-stripping/capture. Many reactions with low energy unstable radioactive ion beams from newly available ISOL facilities are expected to be of similar nature, see e.g. a recent study of the 7Be+58Ni system [37]. The present rather complete data sets for the breakup and transfer-breakup mechanisms for a stable weakly bound nucleus plus the theoretical analysis provide an important benchmark in this respect.

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