Abstract

Machine learning tools provide a significant improvement in sensitivity over traditional analyses by exploiting subtle patterns in high-dimensional feature spaces. These subtle patterns may not be well-modeled by the simulations used for training machine learning methods, resulting in an enhanced sensitivity to systematic uncertainties. Contrary to the traditional wisdom of constructing an analysis strategy that is invariant to systematic uncertainties, we study the use of a classifier that is fully aware of uncertainties and their corresponding nuisance parameters. We show on two datasets that this dependence can actually enhance the sensitivity to parameters of interest compared to baseline approaches. Finally, we provide a cautionary example for situations where uncertainty mitigating techniques may serve only to hide the true uncertainties.

1 Introduction

The usefulness of physical measurements is tied to the magnitude and reliability of their estimated uncertainties. The most troublesome, systematic uncertainties, are often modeled as the dependence of a parameter of interest on other degrees of freedom, nuisance parameters.

In high energy physics, machine learning models are typically trained on synthetic datasets generated with assumed values of the nuisance parameters. We will refer to this as the baseline approach. Several approaches have been considered to incorporate uncertainties into the training. Data augmentation trains a model on a concoction of synthetic data with different values of the nuisance parameters. Another possibility is to train a model to explicitly be insensitive to nuisance parameters [1–15], such as with adversarial training [1–4]. Maximizing overall sensitivity requires a compromise between the level of independence to nuisance parameters and the classification power. These three approaches will serve as important baselines in this paper.
We advocate for the opposite of decorrelation. Classifiers are constructed to be explicitly dependent on nuisance parameters. As nuisance parameters are profiled, the classifier will change and the best classifier will be used for each value of the nuisance parameter. Parameterized classifiers have been studied in the context of parameters or features of interest [16, 17], and full dependence on nuisance parameters for inference has been advocated in Ref. [18–22].

In this paper, we provide specific examples of profiled classifiers and show explicitly that parameterized classifiers can enhance analysis sensitivity over strategies that render networks insensitive to nuisance parameters. We focus on only the construction of classifiers as useful statistics for downstream analysis and not on full likelihood (ratio) estimation. In this way, our uncertainty-aware classifier approach [23] is a straightforward extension of existing analyses performed at the Large Hadron Collider (LHC) and elsewhere, and therefore may result in immediate improvements in sensitivity. In addition, this prescription allows for easy post-hoc histogram-based diagnostics. These may include quantification of the impact of additional sources of systematic uncertainties that are not used for training, and checks for whether the measurement over-constrains the nuisance parameter.

While we focus on the profiling aspect of uncertainty awareness, there is a complementary line of research on the use of inference-aware loss functions [24–30] and Bayesian neural networks for estimating uncertainties [31–34]. We leave the combination of these methods with our uncertainty-aware approach to future work. Additional information about the interplay between uncertainties and machine learning can be found in recent reviews [22, 35].

All the neural networks discussed in this paper were trained using Keras [36] with a Tensorflow backend. Further implementation details are available with the code at https://github.com/hep-lbdl/systaware.

2 Uncertainty-Aware Classifier

The uncertainty-aware network is trained with the true value of the nuisance parameter $z$ as an input to the network in addition to the observables $x$, see Fig. 1. Trained with a Binary Cross-Entropy loss, the network approximates the score,

$$s(x, z) = \frac{p(x|Z = z, S)}{p(x|Z = z, S) + p(x|Z = z, B)},$$

where $p(\cdot)$ denotes a probability density, $S$ represents the signal class and $B$ represents the background class. Note that Eq. 1 depends on $z$, in contrast to the standard search paradigm in which the analysis observables are fixed and the sensitivity to $z$ is evaluated post-hoc.

3 Evaluation Methodology

To evaluate the power of various approaches, we apply them to a common use case, fitting a signal hypothesis in the presence of background, where both signal and background depend on nuisance parameters. For ease of calculations we perform a binned likelihood fit.

For each strategy, template histograms of the classifier score are constructed from simulated signal and background events for several values of the nuisance parameter $z$. These templates are the basis of the binned likelihood calculation $L(\mu, z|\{x_i\})$ over the parameters $\mu, z$, where $\{x_i\}$ is the full observed dataset. The likelihood is a product of a Poisson term for each histogram bin and a Gaussian constraint on the nuisance parameter. The Gaussian constraint can readily be replaced with any other prior or a Poisson term from an auxiliary measurement if $z$ is directly constrained with control region data. The Negative Log-Likelihood (NLL) is (up to an irrelevant constant),

$$-\log L(\mu, z|\{x_i\}) = -\sum_{j=1}^{n_{\text{bins}}} \left[ N_j \cdot \log (\mu s_j + b_j) - \mu s_j - b_j - \log(\Gamma(N_i)) \right] + \left( \frac{z - z_0}{\sqrt{2}\sigma_z} \right)^2,$$

(2)
where $s_j$, $b_j$ are the expected number of signal and background events in bin $j$, respectively, and $N_j$ is the number of events observed in data for that bin. The $\Gamma$ function is the generalized factorial function which can handle decimal values in the simulated test dataset. Although the $\log(\Gamma(N_i))$ term is usually irrelevant, it is not a constant while using an uncertainty-aware network and cannot be ignored.

The fitted value of $\mu$ is obtained by minimizing Eq. 2. Since the measurement of the nuisance parameter is not the final objective, it is in fact the profile likelihood, $\mathcal{L}_p(\mu) = \max_z \mathcal{L}(\mu, z)$, that is the most relevant metric for determining the relative power of the various approaches. As a diagnostic, the parameter of interest may be profiled over instead to check if the measurement over-constrains the nuisance parameter.

### 4 Gaussian Example

We begin with a Gaussian example with a two-dimensional feature space and a single nuisance parameter. Signal events are drawn from Gaussian distributions in the two features, with means at $\cos(z)$ and $\sin(z)$, respectively; the width of each is set to 0.7. Background events are generated in same fashion, but with means for the two features at $-\cos(z)$ and $-\sin(z)$ respectively.

A set of $4.2 \times 10^7$ events are generated at 21 values of $z$ equally spaced between 0 and $\pi/2$ for the signal and background. $z = \frac{\pi}{4}$ is treated as the nominal value. Ten bins are used to construct the template and observed histograms. The parameter of interest is the signal strength $\mu$ with a true value of 1.

**Results:** For some observed data, the NLL (Eq. 2) is calculated as a function of the parameter of interest $\mu$ and the nuisance parameter $z$ for each approach. An example of this two dimensional NLL distribution is shown in Fig. 2, which was computed by comparing templates from the baseline classifier to the "observed data" generated at $z = \frac{\pi}{4}$.

The profile likelihood for each method is shown in Fig. 3 for data generated with $z = \frac{\pi}{2}$. We see that the uncertainty-aware classifier provides the best performance.

### 5 Realistic Example

The study is also performed on datasets [38] produced [39] for the HiggsML Kaggle challenge [40] and later enhanced [41] as benchmark datasets for uncertainty quantification [42, 43]. The nuisance parameter is related to the uncertainty of the measured $\tau$ lepton transverse energy.

**Results:** The performance of the four approaches are compared on data generated at the nominal value of $z = 1$ as well as shifted values of $z = 0.8$ and $z = 1.1$. In addition to these approaches, classifiers trained on data from the shifted values of $z$ are added to the comparisons. The true value of $\mu$ was set to 1 throughout. Thirty bins are used to construct the template and observed histograms.

Figure 4 shows that the uncertainty-aware classifier maintains ideal performance for all values of $z$ while all other approaches are at best able to match the performance only for a single value of $z$.
6 Theory Uncertainties

While incorporating uncertainties in the training is desirable, caution must be taken to include only nuisance parameters with a statistical origin. For example, uncertainties due to fragmentation modelling are often estimated using the difference of two models (PYTHIA and HERWIG), and a full theoretical uncertainty decomposition is unknown. An example [44] of two classifiers trained to identify W boson jets (signal) from quark and gluon jets (background) is shown in Fig. 5, where adversarial training is used to reduce the difference in performance between PYTHIA and HERWIG. By sacrificing separation power, this difference is successfully reduced when compared to the large gap in performances for the nominal classifier. However, the difference in performance to data generated with a third model (SHERPA) remains large in both classifiers, indicating that the true uncertainty will be underestimated in the case of the adversarial classifier if a third independent sample is unavailable.

7 Conclusions

In this paper, we have advocated for uncertainty-aware classifiers where the dependence on nuisance parameter is maximized during training by exploiting parameterized classifiers [16, 17]. Using a Gaussian example and a realistic $H \rightarrow \tau \tau$ example, we have shown that the uncertainty-aware approach outperforms alternative methods that either are unaware of uncertainties or try to reduce the dependence on them during training\(^1\). Our approach is successful because it provides the most effective classifier for all values of the nuisance parameter. This is useful when uncertainties are evaluated and when the nuisance parameter is profiled. It should be straightforward to apply this approach to multiple nuisance parameters although it was demonstrated on a single nuisance parameter in this paper.

\(^1\)Further details can be found in Ref. [23]

Figure 5: Performance of classifiers on data generated from PYTHIA, HERWIG, and SHERPA. Solid lines correspond to the nominal classifier trained with PYTHIA while dotted lines correspond to the adversarial setup using PYTHIA and HERWIG. The bottom panel shows the relative absolute difference with respect to PYTHIA (nominal or adversarial, as appropriate). Note that the lower panel has a logarithmic vertical axis.

Figure 4: Physics Dataset: Profiled NLL curves for all four classifiers evaluated three values of $z$ where the true value of $\mu$ is 1. Narrower curves indicate more precise measurements having accounted for systematic and statistical uncertainties.
We also recommend that caution must be taken in applying uncertainty mitigating solutions along with an explicit example of the possible danger. We show a case where decorrelating the dependence of a classifier to a theoretical uncertainty only serves to hide the size of the true uncertainty\(^2\). While demonstrated for decorrelation, this cautionary tale remains relevant for other uncertainty or inference aware machine learning approaches [18–22, 24–30]. Ultimately, the decision to use the additional feature or not depends on how the test statistic will be used in the analysis.

The uncertainty-aware technique proposed here is a straightforward extension of existing LHC analyses and will require minimal changes or computational overhead. The biggest improvements are expected in analyses limited by experimental systematics. A large number of analyses will fall into this category at the High-Luminosity LHC and beyond.

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