GLOBULAR CLUSTER SYSTEMS. I. $V-I$ COLOR DISTRIBUTIONS

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ABSTRACT

We have compiled data for the globular cluster systems of 50 galaxies from the Hubble Space Telescope Wide Field Planetary Camera 2 archive, of which 43 are type S0 or earlier. In this paper, we present the data set and derive the $V-I$ color distributions. We derive the first four moments of the color distributions, as well as a measure for their nonunimodality. The number of globular clusters in each galaxy ranges from 18 (in NGC 2778) to 781 (NGC 5846). For those systems having more than 100 clusters, seven of 16 (44%) show significant bimodality. Overall, roughly half of all the systems in our sample show hints of a bimodal color distribution. In general, the distributions of the faint galaxies are consistent with unimodality, whereas those of the brighter galaxies are not. We also find a number of systems with narrow color distributions—with both mean red and blue colors—suggesting that systems exist with only metal-rich or only metal-poor globular clusters. We discuss their possible origins. In comparing the moments of the $V-I$ distributions with various galaxy properties for the early-type galaxies, we find the following differences in the correlations between the field and cluster galaxy populations: the peak $V-I$ color of the globular cluster distribution correlates well with the central velocity dispersion—and hence the Mg$_2$ index and total luminosity—for galaxies in cluster environments; there exists no such correlation for field galaxies. This difference between cluster and field galaxies possibly reflects different formation scenarios for their globular cluster systems. Among the explanations for such a correlation, we consider either a larger age spread in the field populations or the possibility that cluster galaxies are always affected by significant accretion whereas some field galaxies could host pure "in situ" formed populations.

Key words: galaxies: elliptical and lenticular, cD — galaxies: star clusters

1. INTRODUCTION

In the past decade, globular cluster systems were established as powerful probes for the formation and evolution of galaxies (see, e.g., Harris 1991 and Ashman & Zepf 1998 for reviews). With very few exceptions, globular clusters exist in large numbers around all galaxies. They are not only easy to detect; their properties are readily influenced by the formation and evolution of their host galaxies and, in a larger sense, their environment. Globular cluster formation is also closely related to the star formation history of the galaxies (see, e.g., Kissler-Patig, Forbes, & Minniti 1998b). The study of globular cluster systems, combined with the predictions of their properties from various galaxy formation scenarios, can therefore be used to constrain galaxy formation and evolution.

In recent years, tens of galaxies have been studied for their globular cluster populations (e.g., the compilation in Ashman & Zepf 1998). However, no systematic study of the properties of globular cluster systems, including more than a dozen hosts, has been carried out. Motivated by the need for a homogeneous study of a large number of systems, we have exploited the archive of the Hubble Space Telescope (HST) as an ideal starting point for such a study, since it includes a large number of images centered on galaxies in different filters and taken in nearly identical conditions, leading to homogeneous photometry.

We begin by studying the properties of globular cluster systems around a large number of early-type galaxies, then describe the resulting sample in § 2 and the pipeline reduction in § 3. We study the color distributions of the systems (presented in §§ 4 and 5) and follow with a discussion of the properties of the color distributions, correlations among these properties, and their relation to the properties of the host galaxies (§§ 6 and 7). Because color represents a mix of age and metallicity of the systems, globular cluster systems have gained considerable interest after the discovery of multimodal distributions in some systems (Zepf & Ashman 1993). Such a system implies that, at least in some galaxies, globular clusters formed from different mechanisms and possibly at several epochs. Color distributions alone are thus already a strong diagnostic for the history of the globular cluster systems and, by implication, for the history of the host galaxies. We discuss the properties of the color distributions of our sample for various formation scenarios in § 8. In a companion paper, we will use these data to constrain the models of Côté, Marzke, & West (1998).

2. THE GALAXY SAMPLE

We searched the HST archive for all early-type galaxies that have been observed in two colors with adequate...
| Galaxy       | Filter | T_{exp} (s) | N_{exp} | PI (Program)                  |
|--------------|--------|-------------|---------|-------------------------------|
| NGC 584      | F555W  | 1520        | 5       | S. M. Faber (6099)            |
|              | F814W  | 1450        | 7       |                               |
| NGC 596      | F555W  | 1600        | 4       | D. Richstone (6587)          |
|              | F814W  | 1800        | 3       |                               |
| NGC 821      | F555W  | 1520        | 5       | S. M. Faber (6099)            |
|              | F814W  | 1450        | 7       |                               |
| NGC 1023*    | F555W  | 2920        | 11      | S. M. Faber, D. Richstone (6099, 6587) |
|              | F814W  | 3780        | 10      |                               |
| NGC 1316     | F450W  | 5000        | 5       | C. Grillmair (5990)          |
|              | F814W  | 1860        | 3       |                               |
| NGC 1399     | F450W  | 5200        | 4       | C. Grillmair (5990)          |
|              | F814W  | 1800        | 3       |                               |
| NGC 1404     | F450W  | 5000        | 5       | C. Grillmair (5990)          |
|              | F814W  | 1860        | 3       |                               |
| NGC 1426     | F555W  | 1600        | 4       | D. Richstone (6587)          |
|              | F814W  | 1800        | 3       |                               |
| NGC 1700     | F555W  | 1600        | 4       | D. Richstone (6587)          |
|              | F814W  | 1800        | 3       |                               |
| NGC 2300     | F555W  | 1520        | 5       | S. M. Faber (6099)            |
|              | F814W  | 1450        | 7       |                               |
| NGC 2434     | F555W  | 1300        | 2       | M. Carollo (5943)            |
|              | F814W  | 1000        | 2       |                               |
| NGC 2778     | F555W  | 1520        | 5       | S. M. Faber (6099)            |
|              | F814W  | 1450        | 7       |                               |
| NGC 3115     | F555W  | 1015        | 6       | S. M. Faber (5512)            |
|              | F814W  | 1236        | 6       |                               |
| NGC 3377     | F555W  | 1330        | 6       | S. M. Faber (5512)            |
|              | F814W  | 1236        | 6       |                               |
| NGC 3379     | F555W  | 1660        | 4       | S. M. Faber (5512)            |
|              | F814W  | 1340        | 4       |                               |
| NGC 3384     | F555W  | 1430        | 6       | S. M. Faber (5512)            |
|              | F814W  | 1290        | 6       |                               |
| NGC 3585     | F555W  | 1200        | 6       | D. Richstone (6587)          |
|              | F814W  | 1900        | 3       |                               |
| NGC 3610     | F555W  | 1400        | 6       | D. Richstone (6587)          |
|              | F814W  | 2100        | 3       |                               |
| NGC 3640     | F555W  | 1200        | 6       | D. Richstone (6587)          |
|              | F814W  | 2100        | 3       |                               |
| NGC 4125     | F555W  | 1400        | 6       | D. Richstone (6587)          |
|              | F814W  | 2100        | 3       |                               |
| NGC 4192     | F555W  | 660         | 3       | V. C. Rubin (5375)           |
|              | F814W  | 660         | 3       |                               |
| NGC 4291     | F555W  | 1520        | 5       | S. M. Faber (6099)            |
|              | F814W  | 1450        | 7       |                               |
| NGC 4343     | F555W  | 660         | 3       | V. C. Rubin (5375)           |
|              | F814W  | 660         | 3       |                               |
| NGC 4365     | F555W  | 2200        | 2       | J. Brodie (5920)             |
|              | F814W  | 2300        | 2       |                               |
| NGC 4374     | F547M  | 1200        | 2       | G. Bower (6094)              |
|              | F814W  | 520         | 2       |                               |
| NGC 4406     | F555W  | 1500        | 3       | S. M. Faber (5512)            |
|              | F814W  | 1500        | 3       |                               |
| NGC 4450     | F555W  | 520         | 3       | V. C. Rubin (5375)           |
|              | F814W  | 520         | 3       |                               |
| NGC 4458     | F555W  | 1340        | 4       | S. M. Faber (5512)            |
|              | F814W  | 1120        | 5       |                               |
| NGC 4472*    | F555W  | 4400        | 4       | J. Brodie (5920)             |
|              | F814W  | 4600        | 4       |                               |
| NGC 4427     | F555W  | 1800        | 3       | S. M. Faber (6099)            |
|              | F814W  | 2000        | 4       |                               |
| NGC 4478     | F555W  | 1600        | 4       | D. Richstone (6587)          |
|              | F814W  | 1800        | 3       |                               |
| NGC 4486     | F555W  | 2810        | 6       | F. D. Macchetto (5477)        |
|              | F814W  | 2430        | 5       |                               |
| Galaxy          | Filter | $T_{\text{exp}}$ (s) | $N_{\text{exp}}$ | PI (Program) |
|-----------------|--------|----------------------|------------------|--------------|
| NGC 4486B...... | F555W  | 1800                 | 3                | S. M. Faber (6099) |
| NGC 4526 ......  | F555W  | 520                  | 3                | V. C. Rubin (5375) |
| NGC 4536 ......  | F555W  | 660                  | 3                | V. C. Rubin (5375) |
| NGC 4550 ......  | F555W  | 1200                 | 3                | V. C. Rubin (5375) |
| NGC 4552 ......  | F555W  | 2400                 | 4                | S. M. Faber (6099) |
| NGC 4569 ......  | F555W  | 520                  | 3                | V. C. Rubin (5375) |
| NGC 4594 ......  | F547M  | 1340                 | 4                | S. M. Faber (5512) |
| NGC 4621 ......  | F555W  | 1380                 | 6                | S. M. Faber (5512) |
| NGC 4649 ......  | F555W  | 2100                 | 2                | J. A. Westphal (6286) |
| NGC 4660 ......  | F555W  | 1000                 | 5                | S. M. Faber (5512) |
| NGC 4881 ......  | F555W  | 7200                 | 8                | J. A. Westphal (5233) |
| NGC 5018 ......  | F555W  | 1200                 | 6                | D. Richstone (6587) |
| NGC 5061 ......  | F555W  | 1200                 | 6                | D. Richstone (6587) |
| NGC 5845 ......  | F555W  | 2140                 | 5                | S. M. Faber (6099) |
| NGC 5846* ...... | F555W  | 6600                 | 6                | J. Brodie (5920) |
| NGC 7192 ......  | F555W  | 1300                 | 2                | M. Carollo (5943) |
| NGC 7457 ......  | F555W  | 1380                 | 6                | S. M. Faber (5512) |
| IC 4889 ..........| F555W  | 600                  | 1                | M. Carollo (5943) |

* NGC 1023 and NGC 4472 have two different pointings; NGC 5846 has three.

exposure times, using only Wide Field Planetary Camera 2 (WFPC2) data from a variety of programs, with the Nuker group (principal investigators S. M. Faber and D. Richstone) providing most of it. Ninety percent of the galaxies were observed in F555W ($V$) and F814W ($I$); some galaxies were observed through the F547M and the F450W filters, which we transformed to $V$ (see below). We did not use data taken in other filters. Although we may have some early-type galaxies, we attempted to make a complete study from the archive. Furthermore, some of the galaxies below are not early-types; we include them only for comparison, not for use in the analysis.

Table 1 presents the data properties for each galaxy: galaxy name, filter, total exposure time, number of individual exposures, and principal investigator name and program number. Three galaxies have more than one pointing, and we include their total exposure times from all pointings. There are 50 galaxies in total. Table 2 summarizes the physical properties for the 43 galaxies that are S0 or earlier.

3. THE PIPELINED REDUCTION

We reduced all of the data starting from the individual exposures. The Canadian Astronomy Data Centre provided the recalibrated science exposure. All data were sent through a pipelined reduction. We divide the reduction into two steps: the combination of the individual images, and the photometry for the globular clusters. The first step requires shifting the images, scaling by exposure times, and combining. We use the HST header parameters for the telescope pointing (CRVAL1 and CRVAL2) to determine the shift. Instead of using the telescope pointing, we could have used reference objects in the images to measure the shift; for a handful of galaxies, we confirmed that the telescope pointing provides the same shift as when we used reference objects. We use a linear shift so as not to smear cosmic-ray-affected pixels, then scale the images to a common exposure time. Different gains were used between galaxies and even among different exposures of the same galaxy. Finally, we transformed all images to gain 7. The combining process must be robust, as many of the galaxies have a limited number of individual exposures, which makes it difficult to remove cosmic rays adequately. We therefore use a biweight estimate for the combining. The biweight attempts to estimate the mode of a distribution by using an iterative

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* See http://cadcwww.dao.nrc.ca for details of the recalibration.


The second part of the reduction includes the photometry. Most of these data have the center of the galaxy in one of the WFPC2 chips (most are in the Planetary Camera). To measure with greater reliability those clusters that have the high-background galaxy under them, we first subtract the galaxy light using a “median filtering” technique; instead of the median, we use a biweight estimate (explained above) for the local flux value. We choose the parameters for the filtering—i.e., the inner radius equals 8 pixels and the outer radius equals 14 pixels—based on results from experiments with no background present. In addition, we make an initial pass to detect the globular clusters, then flag those pixels under the clusters to make sure the filtering technique does not include them when determining the galaxy component. We subtract the galaxy only in the chip that contains the galaxy center.

We use SExtractor (Bertin & Arnouts 1996) for the photometry, setting the finding parameters to 2 connected pixels 2.5 σ over the local background as defined in a 32 × 32 pixel box. The frames were further convolved with the point-spread function kernel given in the WFPC2 handbook for the respective chips in order to optimize the finding (see Bertin & Arnouts 1996).

We must correct the resulting magnitudes since the photometry is measured in a 2 pixel radius aperture. We correct the resulting magnitudes to a 0.5 radius aperture, using the values proposed by Whitmore et al. (1997), and by 0.1 mag in order to extrapolate to the total light (see Holtzman et al. 1995). Finally, the magnitudes measured in the HST filter set were converted into the Johnson-Cousins $V$ and $I$.

**Table 2**

| Galaxy   | Type | $M_V$ | log $σ$ | Mg$_2$ | log $ρ$ | $a_4$ | log $R_p$(pc) |
|----------|------|-------|---------|--------|---------|-------|---------------|
| NGC 584  | E    | -21.16 | 2.34    | 0.29   | 0.42    | 1.50  | 3.51          |
| NGC 596  | Epec | -20.93 | 2.22    | 0.25   | 0.40    | 1.30  | ...           |
| NGC 821  | E    | -20.84 | 2.32    | 0.32   | 0.08    | 2.50  | 3.45          |
| NGC 1023 | SB0  | -20.61 | 2.34    | 0.34   | 0.57    | ...   | 3.26          |
| NGC 1399 | E1 pec | -21.97 | 2.52    | 0.37   | 1.59    | 0.00  | ...           |
| NGC 1404 | E1   | -21.56 | 2.38    | 0.34   | 1.59    | 0.50  | ...           |
| NGC 1426 | E4   | -20.42 | 2.18    | 0.28   | 0.66    | ...   | 3.44          |
| NGC 1700 | E4   | -21.90 | 2.36    | 0.28   | ...     | 0.90  | ...           |
| NGC 2300 | SA0  | -20.76 | 2.42    | 0.33   | 0.14    | -0.60 | 3.58          |
| NGC 2434 | E0   | -20.60 | 2.31    | 0.27   | 0.19    | ...   | 3.49          |
| NGC 2778 | E    | -19.43 | 2.26    | 0.34   | 0.28    | ...   | ...           |
| NGC 3115 | E0   | -20.82 | 2.45    | 0.34   | 0.08    | 8.00  | 3.17          |
| NGC 3377 | E5   | -19.96 | 2.18    | 0.29   | 0.49    | 1.20  | 3.21          |
| NGC 3379 | E1   | -20.83 | 2.35    | 0.34   | 0.52    | 0.10  | 3.23          |
| NGC 3384 | SB0  | -19.89 | 2.21    | 0.29   | 0.54    | ...   | ...           |
| NGC 3585 | E7   | -21.75 | 2.34    | 0.32   | 0.12    | 4.50  | 3.50          |
| NGC 3610 | E5   | -20.92 | 2.21    | 0.27   | 0.30    | 2.50  | ...           |
| NGC 3640 | E3   | -21.75 | 2.24    | 0.27   | 0.18    | -0.20 | ...           |
| NGC 4125 | E6 pec | -22.09 | 2.25    | 0.32   | 0.34    | 1.00  | 3.43          |
| NGC 4291 | E    | -20.69 | 2.43    | 0.32   | 0.36    | -0.40 | 3.64          |
| NGC 4365 | E3   | -22.12 | 2.42    | 0.35   | 2.93    | -1.10 | 3.79          |
| NGC 4374 | E1   | -22.21 | 2.44    | 0.32   | 3.99    | -0.40 | ...           |
| NGC 4406 | S0   | -22.41 | 2.40    | 0.33   | 1.41    | -0.70 | ...           |
| NGC 4458 | E0   | -19.06 | 2.02    | 0.25   | 3.21    | ...   | ...           |
| NGC 4472 | E2   | -22.59 | 2.48    | 0.34   | 3.31    | -0.30 | 3.89          |
| NGC 4473 | E5   | -20.80 | 2.26    | 0.33   | 2.17    | 0.90  | 3.60          |
| NGC 4478 | E2   | -19.94 | 2.13    | 0.27   | 3.92    | -0.80 | ...           |
| NGC 4486 | E0   | -22.48 | 2.56    | 0.30   | 4.17    | 0.00  | 3.89          |
| NGC 4486B | cE0 | -17.75 | 2.30    | 0.30   | 4.17    | ...   | 3.51          |
| NGC 4526 | SB0  | -20.89 | 2.47    | 0.30   | 2.45    | ...   | 3.57          |
| NGC 4550 | SB0  | -18.81 | 2.01    | 0.17   | 2.97    | -0.70 | ...           |
| NGC 4552 | E    | -21.26 | 2.42    | 0.35   | 2.97    | ...   | 3.35          |
| NGC 4621 | E5   | -21.63 | 2.40    | 0.35   | 2.60    | 1.50  | 3.54          |
| NGC 4649 | E2   | -22.31 | 2.56    | 0.37   | 3.49    | -0.50 | 3.74          |
| NGC 4660 | E    | -19.26 | 2.29    | 0.33   | 3.37    | 2.70  | 3.56          |
| NGC 4881 | E    | -21.60 | 2.33    | 0.29   | ...     | ...   | ...           |
| NGC 5018 | E3   | -22.31 | 2.32    | 0.21   | 0.29    | 2.00  | ...           |
| NGC 5061 | E0   | -21.62 | 2.30    | 0.27   | 0.31    | -1.80 | 3.90          |
| NGC 5845 | E    | -19.63 | 2.42    | 0.32   | 0.84    | 0.80  | ...           |
| NGC 6846 | E0   | -22.23 | 2.40    | 0.34   | 0.84    | 0.00  | 3.37          |
| NGC 7192 | SA0  | -21.49 | 2.27    | 0.26   | 0.28    | ...   | 3.71          |
| NGC 7457 | SA0  | -18.25 | 1.76    | 0.19   | 0.13    | ...   | ...           |
| IC 4889  | E5   | -21.26 | 2.22    | 0.26   | 0.13    | 1.00  | ...           |
Fig. 1.—Histograms of the globular cluster systems' $V-I$ colors for all of the galaxies. The solid line represents a density estimate and the dotted lines are the 90% confidence bands. The total number of globular clusters appears under the galaxy name.
Fig. 1.—Continued
Fig. 1.—Continued
system by applying the transformations given in Holtzman et al. (1995). For the F555W and F814W filters used in the vast majority of our data sets, empirical transformations exist. For the F547M filter, we used the theoretical transformation into the $V$ filter. Finally, we used the empirical transformation to convert the F450W filter, used for the Fornax galaxies, into a Johnson $B$ filter, followed by a linear transformation from $B-I$ into $V-I$ derived from the population synthesis models of Bruzual & Charlot (1993) for ages in excess of 5 Gyr and the full range of available metallicities. The linear transformation follows $V-I = 0.466(B-I) + 0.14$. The average uncertainty of the magnitudes is 0.06; this uncertainty scales with magnitude roughly so that at $V = 24$ we have an uncertainty of 0.1, and at $V = 20$ an uncertainty of 0.01. We go down to around 25.5 in $V$ and 24.5 in $I$, but we are only able to approximate both our limiting magnitude and uncertainty, given that the galaxies have a range of exposure times.

We note that the extrapolations from 2 pixel apertures to total magnitudes, derived for point sources, are extremely uncertain when applied to slightly extended objects such as globular clusters and can significantly affect the final magnitudes (see Kundu & Whitmore 1998; Puzia et al. 1999). However, the error of the extrapolation is similar in the F555W and F814W filters, so that the final colors are not affected by systematic errors of less than 0.03 mag.

Finally, the data were corrected for foreground reddening using the maps of Schlegel, Finkbeiner, & Davis (1998) and the law $E(V-I) = 1.55(B-V)$.

4. THE $V-I$ COLOR DISTRIBUTION OF THE SYSTEMS

SExtractor provides an estimate of the magnitude, magnitude error, ellipticity, FWHM, and star/galaxy classification. From these measurements we select globular clusters from the objects that have the following criteria: a magnitude error smaller than 0.1; $V-I$ color between 0 and 2; ellipticity smaller than 0.5; FWHM between 1 and 4 pixels (on both the PC and WF chips); and “nonstar” classification (set to reject remaining cosmic rays and hot pixels, rather than to try to exclude point sources). No cut on the magnitude exists, since it correlates with the magnitude error. The number of true globular clusters excluded by these criteria is typically less than 10%, somewhat higher for the most distant galaxies and those with short exposure times. The contamination by foreground stars and background galaxies passing our selection criteria is roughly constant and estimated from the Hubble Deep Field (Williams et al. 1996). The percentage of contamination depends on the distance and the richness of the globular cluster system considered, lying around 5% for a typical system with over 100 clusters at a distance of 10 to 20 Mpc. It can rise up to 30% to 50% for systems at significantly larger distances—which we then excluded in the following analysis where mentioned—or for systems with significantly fewer clusters.

Figure 1 plots $V-I$ histograms for all of the 50 galaxies in the sample. As a histogram is the crudest form of density estimation, we also include the adaptive kernel density estimate as the solid lines. A histogram is a density estimate that utilizes both discreet and equal-sized windows; it is therefore dependent on both the choice of the window size and the location of the window edges. More robust techniques include both weights for an individual data point’s contribution to a density estimate, and varying size that preserves the noise properties (i.e., sparse regions require larger binning). The adaptive kernel estimate contains these properties and provides a nonparametric density estimate on a grid. We refer to Silverman (1986) for a complete discussion of the adaptive kernel estimate. It works as follows: We obtain an initial density estimate, then adjust the window width at each grid element according to the initial density in such a way that low-density regions have a large window width. We use the Epanechnikov kernel, an inverted parabola, for the density estimate. The result of an adaptive kernel estimate can be highly dependent on the initial smoothing, especially for small samples such as ours with $N < 100$; thus, we use least-squares cross validation to
This technique minimizes an estimate of the integrated square error given by $(\bar{f} - f)^2$, where $f$ is the density estimated from the data—dependent on the window width (the smoothing parameter)—and $\bar{f}$ is the underlying function we are trying to estimate. One point is removed from the sample, and we estimate the density for a given smoothing from the $N - 1$ data points. Repeating this $N$ times and using the average provides an estimate of the underlying function $f$. The optimal smoothing is then the one that minimizes the estimated integrated square error.

The dotted lines in Figure 1 represent the 90% confidence bands obtained through a bootstrap estimate, a technique that draws with replacement from the original sample of $N$ points. One bootstrap realization contains $N$ points, which are not necessarily unique. For each realization we estimate the distribution function and repeat this procedure 1000 times. At each grid element we then have a distribution of points, from which we choose the 5% and the 95% values, representing the 90% confidence band. These confidence bands reflect only the variance, not the bias, of the estimate. The bootstrap procedure includes the measurement uncertainties implicitly because they are reflected in the original estimate of the colors.
4.1. Measuring the Moments of the Distributions

Moments represent a simple quantification of the distributions that we correlate with other galaxy properties (discussed below). However, because of small number statistics and contamination, we desire a more robust estimate for the moments other than the classical estimates. We therefore use the biweight estimate of location (first moment) and scale (second moment), Finch's asymmetry index (third moment), and the tail index (fourth moment). Beers et al. (1990) describe the biweight estimators in detail. The asymmetry index measures skewness by comparing gaps between the ordered data points on both the right and left sides of the distribution. The gaps are weighted according to their rank order, thereby devaluing the contribution from outliers. The tail index measures the spread of the data set at the 90% level relative to the spread at 75% and is normalized such that a Gaussian has an index equal to 1. Bird & Beers (1993) provide an explanation of the asymmetry index and tail index and show that they are superior estimates compared with the classical skewness and kurtosis. Table 3 presents these robust moments and their 68% confidence band. A bootstrap procedure, the same as described above, provides the confidence bands. The galaxies listed in italics in Table 3 are late-type.

5. RELATIONS BETWEEN MOMENTS AND GALAXY PROPERTIES

In the following sections, we investigate the relations among the properties of the globular cluster color distributions and their relation to the properties of the host galaxies. We restrict ourselves to a homogeneous sample of globular cluster systems with best-determined properties. We include S0 and elliptical galaxies, but we exclude the late-type galaxies listed in italics in Table 3. We further restrict the sample to galaxies with redshifts of less than 3000 km s\(^{-1}\) (excluding NGC 1700 and NGC 4881), since at anything smaller than this distance, contaminating foreground/background objects present no problem. We set a lower limit on the number of globular clusters of 50 systems, for which the moments are well defined. Finally, we exclude the systems that were not observed in the F555W and F814W filters, to avoid systematic effects in the conversion to a homogeneous photometric system (excluding NGC 4374, 1399, and 1404).

The restricted sample includes 26 globular cluster systems, for which the distributions of properties are shown in Figure 2, which presents all properties plotted against each other, as we discuss below. The range of the \(V - I\) moments shows a relatively sharp cutoff in the peak color at \(V - I \approx 1.12\). The width or scale appears to be around 0.16 for most systems, including an artificial broadening by photometric errors of around 0.06 typically, with only few systems having significantly broader distributions. Most of the systems are slightly positively skewed—i.e., they have the tendency to cut off more sharply in the blue and extend somewhat toward the red. Finally, the tail index implies that most of the distributions have tail weight consistent with a Gaussian distribution.

5.1. Peak to the Second, Third, and Fourth Moments

We show the relation between the peak and the scale (width) of the distributions in the leftmost plot on the top row in Figure 2; an enlarged version appears in Figure 3. We first note that a blue cutoff is seen in all distributions, implying a lower metallicity limit for all globular clusters. This limitation imposes a lower cutoff in color and forbids a broadening of any distribution toward the extreme blue (about \(V - I < 0.8\)). Therefore, in order to have a blue mean color, systems both must lack those red globular clusters that could not be compensated by extreme blue clusters and must be narrow. Interestingly, such systems with very few red clusters are observed in our sample, i.e., seem to exist among early-type galaxies.

On the other hand, red systems show a wide range of scale values, indicating that both systems with only red clusters (red peak, small scale) and systems with a wide range of globular cluster colors exist. Figure 3 shows that the reddest systems (about \(V - I > 1.1\)) have systematically large scales. These systems must have a broad range of colors, including blue clusters. For systems with \(V - I > 1.1\), a large scale is partly expected as a result of the fact that the \(V - I\) color changes faster with metallicity at high metallicities (see, e.g., Kissler-Patig et al. 1998a; compare with the theoretical predictions, e.g., Worthey 1994) and thus broadens any distribution.

The comparisons of the peak color with either the skewness or the tail indicate no significant trends. The exception is expected: if a blue system is strongly skewed, the skewness is toward the red color, and vice versa. However, not only do most systems fail to show a strong skewness, the tail weights of the color distributions do not deviate much from a Gaussian and show no systematic trends.

5.2. Properties of the Host Galaxies

For the host galaxies, we compiled a number of properties to correlate with the properties of the globular cluster color distribution. These galaxy properties are given in Table 2, together with the source. The galaxy properties include type, total luminosity, total color, central velocity dispersion, central Mg\(_{\text{II}}\) index, environment density, isophotal shape parameter, and, when applicable, effective radius.

The distribution of the properties for the 26 galaxies appear in the plots on the lower right side of Figure 2. The vast majority are elliptical galaxies. We separate field from cluster galaxies at a density parameter of \(\rho = 1\); i.e., galaxies in groups such as Leo (NGC 3377, 3379, 3384) will belong to the field, while galaxies in small or medium-sized clusters, such as Fornax and Virgo, will belong to the cluster category. We thus have 15 galaxies belonging to the field (Fig. 2, triangles) and 11 belonging to the cluster category (circles).

While the Mg\(_{\text{II}}\)-\(\sigma\) relation is well defined for our galaxies, the Faber-Jackson relation shows significant scatter, probably as a result of noise in the distances. Therefore, we use the central velocity dispersion as a distance-independent measure for the relative galaxy mass, rather than the absolute magnitude. We have also made comparisons using \(\log r_e \sigma^2\), which should reflect the galaxy mass better than the dispersion alone, and find no better correlations.

5.3. Correlations with the Whole Sample

We first consider the whole sample, independent of environment. No significant correlation between the peak or scale of the globular cluster systems and any galaxy property could be detected, as measured by the Spearman rank-order correlation coefficients. We note only that boxy
galaxies \((a/a_4 < 0)\) have systematically red peaks and that
the peak values scatter most for intermediate galaxies when
plotted against \(M_V, \sigma,\) or \(M_{g2}\) of the host galaxies.

At face value, this result might contradict the known
dependence of the mean metallicity of globular cluster
systems from galaxy luminosity (e.g., Harris 1991; Forbes,
Brodie, & Grillmair 1997a), insofar as brighter galaxies host
globular clusters with a higher mean metallicity. Therefore,
we could have expected a systematically redder peak with
increasing \(M_V\) or \(\sigma\) of the host galaxy. But Ashman & Zepf
(1998) noted that the mean color of the clusters does not
correlate with the galaxy luminosity for early-type galaxies.

In fact, the relation between mean cluster metallicity and
host galaxy luminosity (see Harris 1991) results from the
fact that dwarf galaxies possess relatively less metal-rich
globular clusters than do spirals, which themselves host
relatively less metal-rich globular clusters than giant early-
type galaxies. Within a given galaxy type, the relation
between mean cluster metallicity and galaxy luminosity is
much less clear, if present at all.

5.4. Comparing Field and Cluster Galaxies

The recent models of hierarchical clustering formation
for galaxies (Kauffmann 1996; Baugh, Cole, & Frenk 1996)
predict significant differences in the formation and star formation histories for field and cluster galaxies. For this reason, we investigate these two classes separately and split our samples of galaxies into field and cluster galaxies, as described above.

According to the Spearman rank-order correlation coefficients, no correlations are detected in the field sample of 15 galaxies. However, for cluster galaxies, the peak values are found to correlate positively with the host galaxy velocity dispersions at the greater than 99% confidence level and, accordingly, at greater than 98% confidence level with their \( M_g \) index values. Peak versus galaxy velocity dispersion appears in the seventh plot on the top row of Figure 2 for field and cluster galaxies; an enlarged version is shown in Figure 3. The same results are true when using the total galaxy magnitude—i.e., cluster galaxies show a correlation, whereas the field galaxies do not.

6. BIMODALITY

Tests for bimodality are difficult to quantify. In many of the past studies of globular cluster systems, authors have used double-Gaussian fits to decide whether the system is bimodal. However, these results are highly dependent both on the underlying assumption of Gaussianity and on the criteria for deciding the number of subpopulations. More general tests exist in the statistics literature that impose global conditions on unimodality with no underlying assumptions about the subpopulations. Here, we use the dip statistic (Hartigan & Hartigan 1985). The dip test measures the maximum distance between the empirical distribution function and the best-fitting unimodal distribution, with the significance level based on simulations. Table 3 lists the value for the significance of the dip statistic, but not the DIP value itself. The same is true in Figures 2 and 4, where we plot the significance value only. A significance of 0.9 implies a 90% probability that the distribution is not unimodal. We do not calculate values below 0.5, as the dip statistic is only defined to discriminate against unimodality.

Figure 4 presents the DIP probabilities and confidence bands for all of the galaxies. Out of 43 galaxies for which the dip can be measured, nine show clear deviation from unimodality. These are NGC 1399, 1404, 1426, 3640, 4472, 4486, 4526, 4649, and 5846. Six of these were already known from ground or space studies to show several distinct populations (NGC 1399, Forbes et al. 1998; Ostrov, Forte, & Geisler 1998; Kissler-Patig et al. 1997a; NGC 1404, Forbes et al. 1998; NGC 4472, Geisler, Lee, & Kim 1996; Puzia et al. 1999; NGC 4486, Whitmore et al. 1995; Elson & San-
Fig. 5.—$V-I$ distributions and their 90% confidence bands for the globular clusters combined across galaxies; we use two bins for each of the named galaxy properties. Each line represents an adaptive kernel estimate of the density with unity area.

tiago 1996; NGC 4649, Neilsen & Tsvetanov 1999; NGC 5846, Forbes, Brodie, & Huchra 1997b). Using a test to discriminate between single and double Gaussians, Neilsen & Tsvetanov (1999) found significant bimodal populations in four of their eight galaxies studied. Using the same data sets, we confirm most of their measurements of bimodality; we disagree only on NGC 4552, where we find no evidence of it.

**TABLE 4**

| Subsample          | Range         | $N_G$ | $N_{GC}$ | $V-I$ Peak | Scale | Skewness | Tail | DIP   |
|--------------------|---------------|-------|----------|------------|-------|----------|------|-------|
| Faint              | $M_V > -20.70$| 15    | 803      | 0.019      | 0.028 | 1.019    | 0.182| 0.192 |
| Bright             | $M_V < -21.75$| 13    | 2737     | 0.071      | 0.083 | 0.172    | -1.397| 0.884 |
| Low $\sigma$      | $\log \sigma < 2.3$ | 16    | 872      | 1.041      | 0.051 | 0.187    | 1.024| 0.759 |
| High $\sigma$     | $\log \sigma > 2.4$ | 12    | 2992     | 0.075      | 0.080 | 0.173    | -0.455| 0.879 |
| Low Mg$_2$        | Mg$_2 < 0.30$ | 18    | 1496     | 0.069      | 0.078 | 0.206    | -1.040| 0.968 |
| High Mg$_2$       | Mg$_2 > 0.34$ | 15    | 2597     | 1.070      | 0.064 | 0.176    | -0.292| 0.883 |
| Low $\rho$        | $\log \rho < 1.0$ | 24    | 2202     | 0.071      | 0.056 | 0.200    | 1.306| 0.864 |
| High $\rho$       | $\log \rho > 1.0$ | 17    | 3441     | 0.069      | 0.064 | 0.170    | -0.262| 0.862 |
A further 11 galaxies show DIP values greater than 0.5 at the 1 to 2 \( \sigma \) level—i.e., have potential deviations from unimodality. These are NGC 584, 596, 821, 1023, 2434, 2778, 3115, 3610, 4365, 4458, and 4478. The studies of Neilsen & Tsvetanov (1999) and Kissler-Patig, Brodie, & Minniti (1999) show that NGC 4478 does not seem to have two clearly distinct populations. In contrast, the recent study by Kundu & Whitmore (1998) reveals that NGC 3115 hosts two distinct populations. We speculate that at least some of these systems might have several distinct populations. Further detailed analyses are required for these candidates.

The remaining 23 galaxies do not show deviations from unimodality. We note that the detection of a dip does not correlate with the number of globular clusters detected; the sample size is taken into account when computing the significance of the statistic.

In Figure 2, the bimodality plots of interest are those that show DIP significance versus both the absolute magnitude and the environment density of the host galaxy. The detection of bimodality does not seem to correlate with the environment. However, some trend can be seen with absolute magnitude: low-luminosity systems \((M_V > -20)\) appear unimodal. This trend has already been noted by Kissler-Patig (1997) in relation to other differences between low- and high-luminosity systems. It is not clear yet how much of these differences can be associated with fundamental differences between the two types of galaxies, and how much is just a bias in the observations. Indeed, if the blue peak is constant in all galaxies while the red one scales with galaxy luminosity, the two peaks will be harder to disentangle in fainter galaxies (see Kissler-Patig et al. 1998b). On the other hand, high-luminosity systems do not appear to show bimodality systematically. We note the interesting cases of NGC 4406 (M86) and NGC 4374, two giant elliptical galaxies in Virgo. The first galaxy, a central giant elliptical dominating an infalling group (Schindler, Binggeli, & Böhringer 1999), is clearly unimodal. NGC 4374 also has a unimodal distribution; however, it is heavily skewed to the red, so that a large number of red (presumably metal-rich) globular clusters exist but seem to form a continuous distribution rather than a distinct population.

In summary, it seems harder to rule out the presence of several populations than to detect them. In our sample, roughly half the systems show multiple populations of globular clusters, independently of the environment but preferentially in the brightest galaxies. Our future challenge will be to confirm or rule out single populations in low-luminosity systems.

7. COMBINING GALAXY SAMPLES

The moments of the \( V - I \) distributions are not well estimated in many of our galaxies, based on small numbers of globular clusters. To compare correlations more robustly, we combine the different globular cluster samples to give better estimates of the moments. Because we do not have to exclude galaxies based on there being a small number of measured globular clusters, we now have 43 galaxies in the combined sample. We use the four main parent galaxy properties—magnitude, \( \sigma \), \( \text{Mg}_2 \) index, and density environment—for this analysis, breaking the sample into two bins. Figure 5 plots the results for the combined \( V - I \) distributions. Table 4 presents the various cuts used for the combined samples and the moments and DIP probability for each subsample. Table 4 also presents the number of galaxies and the number of globular clusters in each subsample. Each subsample has more than 800 clusters in which the noise from the moment estimation is minimal. The choice for the cuts in the subsamples results from our inspection of the particular distribution; we attempted to find a clear division between the samples, and when none was apparent, we used cuts that had roughly equal range among the particular variable. The cuts are partly subjective, but the results do not depend strongly on them.

The central location of the \( V - I \) peak is statistically different only in the division between faint and bright galaxies. The faint galaxies have a peak around 0.94, and the bright galaxies have a peak around 1.13. For the other divisions, the \( V - I \) peaks are similar, but the tail indexes differ significantly. Either faint galaxies, low \( \sigma \), low \( \text{Mg}_2 \), or low density causes the \( V - I \) distribution to have significantly more tail weight than compared with their counterpart sample.

The most extreme differences between the combined samples result from the DIP probability. Galaxies that are faint or have low \( \sigma \) or low \( \text{Mg}_2 \) are consistent with a unimodal distribution, whereas their counterpart samples are highly nonunimodal. This effect is also seen when looking at individual galaxies (see § 6 above), and it appears to be a fundamental property of galaxies.

8. DISCUSSION

8.1. The Color Distributions

An important discovery in the study of globular clusters systems over the last decade is the fact that the globular clusters' color distribution in many elliptical galaxies shows several peaks (Zepf & Ashman 1993). This property has been interpreted as reflecting the presence of several distinct populations of globular clusters around the host galaxy. The origin of these different populations is still under debate and might well have several causes. The original explanation argues that spiral-spiral mergers provide old globular clusters from the progenitors, as well as producing a new population during the merger (Ashman & Zepf 1992; see also Schweizer 1987). However, the accretion of enough dwarf galaxies with metal-poor clusters will also obviously build up a distinct metal-poor population. Côté et al. (1998) and Hilker, Infante, & Richtler (1999) investigated this idea. Yet another process involves the pregalactic formation of metal-poor clusters as the building blocks of galaxies, followed by the formation of more metal-rich globular clusters during the collapse of the galaxy (see Kissler-Patig 1997; Kissler-Patig et al. 1998b). Only slightly different is the theory that galaxies formed all their globular clusters in situ and had two main phases of star formation (e.g., Forbes et al. 1997a; Harris, Harris, & McLaughlin 1998; Harris, Harris, & Poole 1999). Today's challenge is to discriminate between the various scenarios with detailed comparison with the present data.

The diversity of the color distributions present in our sample indicates that the scenario is indeed complex. We discuss in turn some of the groups:

1. Galaxies that host "only red clusters," i.e., those having a red peak and a small scale value. The existence of a blue population in these galaxies is not excluded but is unlikely to be significant. The favored scenario for these galaxies is that a single dominant collapse created a bulge and a red population of clusters. We cannot rule the accre-
tion scenario out if these galaxies were formed in an environment poor in material suitable for accretion (e.g., dwarf galaxies; see Chapelon et al. 1999). These galaxies would then be in low-density environments or in the outskirts of clusters; neither is confirmed or ruled out by our present statistics. Finally, the merger scenario could also work for these galaxies if the progenitors were poor in blue clusters. If the merger happened at early times, the progenitors could be still in a gaseous form or, alternatively, could be low surface brightness galaxies for late mergers in the field that host a large amount of gas but apparently few clusters. However, a scenario with gaseous mergers at early times is hard to distinguish from the two-stage in situ scenario.

2. Galaxies that host “only blue clusters,” i.e., that have a blue peak and a small scale value. These galaxies do not seem to host a significant population of red (presumably metal-rich) clusters. In this case, none of the above scenarios would easily be able to explain such systems; one would have to advocate the formation of bulge stars without the formation of clusters. More likely is a “blue” red peak, either because the red clusters formed with a low metallicity or because they have a significantly younger age (about half as old as the true blue clusters; see Kissler-Patig et al. 1998b) that makes them appear blue. In these last two cases, all scenarios work, with some preference to the merger scenario in the frame of hierarchical clustering models that predict late mergers in the field.

3. Galaxies with broad or bimodal color distributions, i.e., that presumably host a comparable amount (say, within a factor of about 3) of blue and red clusters. These are the cases for which the scenarios described above were designed, and we refer to the respective papers for the pros and cons.

Finally, we note that as long as some information is missing (e.g., merger epoch, globular cluster formation mechanisms, the faint end of the luminosity function in different environments), and given the diversity of scenarios, it seems that not always is the same mechanism the dominant one.

8.2. Field and Cluster Systems

Although based on small number statistics, field and cluster early-type galaxies seem to differ in the properties of their globular cluster systems. Whereas cluster galaxies show a correlation between peak value and the galaxy size (as measured by the velocity dispersion), such a relation must be ruled out for field galaxies.

For cluster elliptical galaxies, the recent spectroscopic studies (Cohen, Blakeslee, & Ryzhov 1998; Kissler-Patig et al. 1998a) show that all globular clusters are old (around 10 Gyr or older). At these ages, the clusters can be considered coeval with respect to the influence of their ages on color. Color differences can therefore be interpreted as almost pure metallicity differences, and the relation between peak color and galaxy luminosity might reflect the equivalent of the $M_g$ relation for galaxies. Forbes et al. (1997a) suggest that in systems with two distinct globular cluster populations, the mean metallicity of the red clusters correlates with the luminosity of the host galaxy; the blue peak does not. Their conclusion implies that the correlation of the total sample’s mean color with galaxy size is driven by the metal-rich globular clusters only. Consequently, this would support scenarios in which the metal-poor globular clusters formed in events uncorrelated with their future host galaxy—e.g., in systems that are separate entities from their future hosts. On the other hand, the same research suggests that the metal-rich globular clusters formed in events correlated with the future host galaxy—e.g., the formation of a bulge in a collapse or merger event. In addition, this correlation suggests that the blue subpopulations have roughly a constant color, while for the red population both the peak shifts and the scale increase as a function of color.

Perhaps surprisingly, the peak color of globular clusters in field galaxies does not correlate with the velocity dispersion (approximately, size) of their host galaxy. This result appears to be in contrast with the observation that field and cluster galaxies exhibit a similar $M_g$ relation (Bernardi et al. 1998). We see several possible explanations.

A first alternative might be that the correlation for cluster galaxies is artificial. We verified that it is not caused by sampling different regions in the different galaxies. Indeed, the ratio of blue to red globular clusters does vary with radius (Geisler et al. 1996; Kissler-Patig et al. 1997b; Puzia et al. 1999). Furthermore, the WFPC2 field samples the outer parts less in larger galaxies than in small ones, so that the relative ratio of blue to red galaxies is systematically smaller in large galaxies at fixed field of view. Puzia et al. (1999) tested the importance of this effect on NGC 4472, which has exposures centered on the galaxy as well as pointings that are offset several arcminutes north and south. The respective peaks of the blue and red populations do not change with radius within the errors; however, the varying ratio of blue to red causes the overall peak to shift by 0.02 mag from the inner to the outer field. The effect is too small, though, to explain any systematic correlation. Moreover, in our sample, field and cluster galaxies span different values of galaxy $I$. Where cluster galaxies are of intermediate to giant size, the field galaxies span the low-to-intermediate size range. If indeed intermediate and giant early-type galaxies differ (see above; cf. Kissler-Patig 1997), the presence or absence of a correlation would be due not to environment, but rather to a function of the galaxy size. For example, one could speculate that small galaxies are not surrounded by a “halo” of blue clusters, thus showing a small trend of system peak with size. Intermediate-size or larger galaxies might or might not have such a halo of blue clusters, complicating the interpretation of the peak color and introducing a scatter due to the possible existence of blue clusters. Giant elliptical galaxies would always have blue clusters and a significant redder population that correlates with galaxy size, leading to an overall trend of peak color with galaxy size again. In other words, the correlation would be an artifact of the mix of populations that show a correlation with environment, rather than a physical difference in the enrichment histories.

A second alternative would be a physical interpretation of the result. Thus, the presence of an $M_g$ relation in field and cluster galaxies but absence or presence, respectively, of a peak-$I$ relation would indicate that stars and globular clusters are coupled in cluster galaxies but not in field galaxies. We regard this alternative as unlikely, however, since cluster formation and star formation appear to go together.

Finally, $M_g$ and $V-I$ color could vary differently with age and metallicity. The variations of $M_g$ with age and metallicity are still uncertain, and if, for example, the metal-
rich populations in field elliptical galaxies show a large spread in age from galaxy to galaxy, a trend could mimic an Mg$_2$-σ relation in the field but not a peak-σ relation. In contrast, since all globular clusters in cluster galaxies are old, such a trend would not be present, and both Mg$_2$ and peak would trace metallicity only. Clearly, such speculations require a much better understanding of the influence of age and metallicity on the properties of composite stellar populations. Detailed studies of the ages and metallicities of the systems are needed.

9. SUMMARY AND OUTLOOK

The results presented in this paper suggest that we can use globular cluster systems to study the merger/formation history of both a system itself and its host galaxy. The differences we see between the field and cluster systems suggest that the cluster galaxies are more influenced by accretion, whereas the field systems may be the result of “in situ” globular cluster formation. Combining this result with the strong signature of multimodality seen in many of the systems provides an observational comparison with the various formation scenarios. In a companion paper (Côté et al. 1999), we will compare these results with the theoretical predictions of Côté et al. (1998). More detailed studies of the systems that are candidates for bimodal distributions are underway, including follow-up near-infrared photometry and multiobject spectroscopy. All photometry results are available from the authors.

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REFERENCES

Ashman, K. M., & Zepf, S. E. 1992, ApJ, 384, 50
———. 1998, Global Cluster Systems (Cambridge: Cambridge Univ. Press)
Baugh, C. M., Cole, S., & Frenk, C. S. 1996, MNRAS, 283, 1361
Beers, T. C., Flynn, K., & Gebhardt, K. 1990, AJ, 100, 32
Bernardi, M., Renzini, A., da Costa, L. N., Wegner, G., Alonso, M., Pellegrini, P. S., Rite, C., & Willmer, C. N. A. 1998, ApJ, 508, L143
Bertin, E., & Arnouts, S. 1996, A&AS, 117, 393
Bird, C. M., & Beers, T. C. 1993, AJ, 105, 1596
Bruzual A., & Charlot, S. 1993, ApJ, 405, 538
Chapelon, S., Buat, V., Burgarella, D., & Kissler-Patig, M. 1999, A&A, 346, 721
Cohen, J. G., Blakeslee, J. P., & Ryzhov, A. 1998, ApJ, 496, 808
Côté, P., et al. 1999, in preparation
Côté, P., Marzke, R., & West, M. J. 1998, ApJ, 501, 554
Elson, R. A. W., & Santiago, B. X. 1996, MNRAS, 280, 971
Forbes, D. A., Brodie, J. P., & Grillmair, C. J. 1997a, AJ, 113, 1652
Forbes, D. A., Brodie, J. P., & Huchra, J. P. 1997b, AJ, 113, 887
Forbes, D. A., Grillmair, C. J., Williger, G. M., Elson, R. A. W., & Brodie, J. P. 1998, MNRAS, 293, 325
Geisler, D., Lee, M. G., & Kim, E. 1996, AJ, 111, 1529
Harris, G. L. H., Harris, W. E., & Poole, G. B. 1999, AJ, 117, 855
Harris, W. E. 1991, ARA&A, 29, 543
Harris, W. E., Harris, G. L. H., & McLaughlin, D. E. 1998, AJ, 115, 1801
Hartigan, J. A., & Hartigan, P. M. 1985, Ann. Stat., 13, 70
Hilker, M., Infante, L., & Richtler, T. 1999, A&AS, 138, 55
Holtzman, J. A., Burrows, C. J., Casertano, S., Hester, J. J., Trauger, J. T., Watson, A. M., & Worthey, G. 1995, PASP, 107, 1065
Kauﬀmann, G. 1996, MNRAS, 281, 487
Kissler-Patig, M. 1997, A&A, 319, 83
Kissler-Patig, M., Brodie, J. P., & Minniti, D. 1999, in preparation
Kissler-Patig, M., Brodie, J. P., Schroder, L. L., Forbes, D. A., Grillmair, C. J., & Huchra, J. P. 1998a, AJ, 115, 105
Kissler-Patig, M., Forbes, D. A., & Minniti, D. 1998b, MNRAS, 298, 1123
Kissler-Patig, M., Kohle, S., Hilker, M., Richtler, T., Infante, L., & Quintana, H. 1997a, A&A, 319, 470
Kissler-Patig, M., Richtler, T., Storm, J., & Della Valle, M. 1997b, A&A, 327, 503
Kundu, A., & Whitmore, B. C. 1998, AJ, 116, 2841
Neilsen, E. H., Jr., & Tsvetanov, Z. I. 1999, ApJ, 515, L13
Ostrov, P. G., Forte, J. C., & Geisler, D. 1999, AJ, in press
Puzia, T. H., Kissler-Patig, M., Brodie, J. P., & Huchra, J. P. 1999, AJ, in press
Schindler, S., Binggeli, B., & Bühringer, H. 1999, A&A, 343, 420
Schlegel, D. J., Finkbeiner, D. P., & Davis, M. 1998, ApJ, 500, 525
Schweizer, F. 1987, in Nearby Normal Galaxies, ed. S. M. Faber (New York: Springer), 18
Silverman, B. W. 1986, Density Estimation for Statistics and Data Analysis (New York: Chapman & Hall)
Whitmore, B. C., Miller, B. W., Schweizer, F., & Fall, S. M. 1997, AJ, 114, 1797
Whitmore, B. C., Sparks, W. B., Lucas, R. A., Macchetto, F. D., & Biretta, J. A. 1995, ApJ, 454, L73
Williams, R. E., et al. 1996, AJ, 112, 1335
Worthey, G. 1994, ApJS, 95, 107
Zepf, S. E., & Ashman, K. M. 1993, MNRAS, 264, 611