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Abstract DEAP-3600 is a liquid-argon scintillation detector looking for dark matter. Scintillation events in the liquid argon (LAr) are registered by 255 photomul-
tiplier tubes (PMTs), and pulseshape discrimination (PSD) is used to suppress electromagnetic background events. The excellent PSD performance of LAr makes it a viable target for dark matter searches, and the LAr scintillation pulseshape discussed here is the basis of PSD.

The observed pulseshape is a combination of LAr scintillation physics with detector effects. We present a model for the pulseshape of electromagnetic background events in the energy region of interest for dark matter searches. The model is composed of a) LAr scintillation physics, including the so-called intermediate component, b) the time response of the TPB wavelength shifter, including delayed TPB emission at $\mathcal{O}(\text{ms})$ time-scales, and c) PMT response.

TPB is the wavelength shifter of choice in most LAr detectors. We find that approximately 10% of the intensity of the wavelength-shifted light is in a long-lived state of TPB. This causes light from an event to spill into subsequent events to an extent not usually accounted for in the design and data analysis of LAr-based detectors.

1 Introduction

Several ongoing and planned particle physics experiments, in particular those looking for rare interactions, use liquid argon (LAr) as a particle detection medium [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]. Liquid argon is a bright scintillator that allows for excellent separation of electromagnetic interactions (electron-recoils) from nuclear-recoil events even at low energies, based on differences in the scintillation pulseshape [11, 12]. The pulseshape is the probability of photon detection as a function of time. Understanding the effects that influence features of the pulseshape helps with optimising the pulseshape discrimination (PSD) algorithm, and informs detector design and analysis choices.

The LAr pulseshape is well-known to have a double-exponential time structure originating from a short-lived singlet and a long-lived triplet state [13, 14, 15]. In addition, an intermediate component, which affects the pulseshape between approximately 30 ns to 100 ns, is commonly observed [16, 17, 12, 18, 19]. Some authors attributed this component to late emission of the wavelength shifter 1,1,4,4-tetraphenyl-1,3-butadiene (TPB) [20], making it an instrumental effect. However, the intermediate component was also observed in [19], where the pulseshape was measured without the use of a wavelength shifter. This supports the hypothesis that the intermediate component is a feature intrinsic to LAr scintillation physics.

TPB absorbs the 128 nm LAr scintillation photons and re-emits them at a peak wavelength of 420 nm [21, 22], where photon detection is easier. The TPB emission time is usually considered to be comparable to the LAr singlet decay time. TPB re-emission components at timescales much larger than $\mathcal{O}(\text{ns})$ (larger than the timescale of the intermediate component) were first reported for excitation with alpha particles [23, 24], and more recently at $\mathcal{O}(\text{ms})$ timescales also for excitation with UV light [20, 25, 26]. Those measurements were done in dedicated small-scale setups. The intensity of this delayed TPB emission component is much smaller than that of the LAr triplet decay time close to the event peak, so that it is not a dominant effect in analysis. However, because it is so long lived, it causes light from one event to spill into subsequent events, which does result in a noticeable effect on for example the energy calibration.

This work corroborates the model from [19], which attributes the intermediate component to a feature intrinsic to LAr, and confirms the existing evidence for delayed TPB emission. Both are measured for the first time here in a large LAr-based particle detector.

The pulseshapes contain information on the LAr excimer decay itself but also on detector properties. Once the contributions to the pulseshape are understood, it can be used to extract a) the LAr triplet lifetime, which serves as purity monitor for the LAr target, and b) the magnitude of instrumental effects, to monitor the stability of the light collection and detection system.

We discuss the scintillation pulseshape from $^{39}\text{Ar}$ beta decays, as measured in the DEAP-3600 single-phase LAr dark matter detector [27], starting at the time of the event peak out to 160 ns. We focus on overall effects dominating the pulseshape in different time windows, and disregard or simplify subdominant systematic effects to obtain the simplest model that describes the overall observed features well enough to inform analysis and simulation of DEAP data.

2 The DEAP-3600 detector

The DEAP-3600 detector is described in detail in [27]. We limit the description here to only the parts relevant to this work.

The centre of the DEAP-3600 detector is a spherical volume 170 cm in diameter, which contains 3.3 tonnes of LAr. The scintillation light created in the LAr travels through the argon volume until it reaches the surface of the acrylic vessel (AV) containing the argon. The inside acrylic surface is coated with a 3 μm thick layer of the organic wavelength shifter TPB [28]. The wavelength-
shifted scintillation light is transmitted to the light detectors through a total of 50 cm of acrylic in the form of the AV and acrylic light guides. The 255 cylindrical light guides protrude radially from the acrylic vessel.

A Hamamatsu R5912 high quantum efficiency photomultiplier tube (PMT) is optically coupled to the end of each light guide. The PMTs are shielded from magnetic fields by individual FINEMET® collars, and by magnetic compensation coils located just outside the detector. Additional copper collars prevent large temperature gradients across the length of the PMTs. The PMTs operate at temperatures from −20°C to 5°C.

3 The pulseshape

$^{39}$Ar is a β-emitter that occurs naturally in the atmospheric argon used in the DEAP-3600 detector. The $^{39}$Ar β decays provide a high-statistics sample of LAr scintillation in response to electrons with energies between the trigger threshold of the detector and the $^{39}$Ar endpoint at 565 keV$_{ee}$ [30]. We select events in the approximate energy window used for dark matter search, between 13 keV$_{ee}$ and 40 keV$_{ee}$ for this analysis. The unit keV$_{ee}$ refers to the energy scale for electromagnetic interactions. It is related to the energy scale for nuclear recoil events through the quenching factor [31].

In DEAP-3600, a trigger is generated and data are collected when a total charge equal to the mean charge of approximately 19 photoelectrons is detected in a sliding 177 ns window. Upon triggering on an event, the data acquisition system (DAQ) records the voltage on each PMT every 4 ns. The digitization is set such that the event peak occurs approximately 2.5 μs into the digitized PMT traces. Normal dark matter search data have a 16 μs long event window. For the analysis presented here, approximately 36 hours of data were recorded with a 200 μs long window. The DAQ does not re-trigger within the digitization window of an event, even if the trigger condition is met again.

A pulse-finding algorithm is applied to the digitized PMT traces to find the charge and time of each pulse. The pulse charge is converted to photoelectrons through division by the average single-photoelectron charge of the PMT. The resulting variable, called qPE, contains the pulse charge, less than 3 photons detected in the first 1.6 μs of the trace, an event time close to the DAQ trigger time, and at least 20 μs (for 16 μs long traces) or 200 μs (for 200 μs long traces) elapsed since the previous triggered event.

Figure 2 shows the pulseshape in two energy windows. The histograms are normalized to show rate per PMT. The event peak at $t = 0$ ns, dominated by the LAr singlet and intermediate decay, is followed by the LAr triplet decay-dominated region up to approximately 5 μs. Features at approximately 6.5 μs and 13 μs are due to PMT dark noise and afterpulsing. At $t \geq 14$ μs, the light intensity is still an order of magnitude above the PMT dark noise level, and scales with the event energy as expected for light correlated with the event. Even 160 μs after the event peak, the light level has not subsided to the level of PMT dark noise, though the intensities from both energy windows approach the same level here. This indicates the presence of a source of noise in addition to uncorrelated PMT dark noise. The dark noise rate is taken

In this analysis, we consider events with a total number of qPE from 100 qPE to 300 qPE. Only in this section, a pulseshape from events with 500 qPE to 800 qPE is also shown. The PMT response is linear at these low numbers of qPE. Events additionally had to pass the following data quality cuts: i) low-level: e.g. stable baselines on all PMTs and success of pulse-finding algorithm, ii) reconstructed event position: inside the bulk of the LAr volume, far enough from the surface that no PMT sees more than 20% of the total light in the event, iii) pile-up cuts: only a single event peak in the pulseshape, less than 3 photons detected in the first 1.6 μs of the trace, an event time close to the DAQ trigger time, and at least 20 μs (for 16 μs long traces) or 200 μs (for 200 μs long traces) elapsed since the previous triggered event.
from Fig. 3 and will be discussed together with the origin of the additional noise component in Sect. 4.4.

\[ I_{\text{TPB}}(t) = (1 - R_{\text{TPB}}) \delta(t) + \frac{R_{\text{TPB}} \cdot N_{\text{TPB}} \cdot e^{-2t/\tau_T}}{1 + A_{\text{TPB}}[Ei(-\frac{t + t_a}{\tau_T}) - Ei(-\frac{t}{\tau_T})]^{2}(1 + t/t_a)}. \]

where \( N_{\text{TPB}} \) is a normalization to make the integral of \( I_{\text{TPB}}(t) \) equal to 1, \( R_{\text{TPB}} \) is the probability that the photon will be re-emitted late, and \( Ei \) is the exponential integral. We refer the reader to [25] for more detailed explanation of the terms in the equation.

4.3 Detector geometry and PMT noise

The geometry of the DEAP-3600 detector results in a characteristic photon time distribution due to scattering [35], with the intensity of observed photons dropping to 10% of the maximum within approximately 15 ns. Once a photon hits a PMT, the signal from the resulting photoelectron can be delayed when photoelectrons recoil on a dynode instead of, or in addition to, releasing secondary electrons. The resulting double and late pulsing in the PMTs causes an approximately gaussian peak centered at 58 ns after the nominal arrival time.

The time structures from scattering and double/late pulsing are further smeared with the uncertainty in the
event peak time. The ability of the pulse finder to separate pulses that are close in time also affects the pulse shape, though to a lesser degree.

Photon scattering, early pulsing, and late/double pulsing all occur at the same prompt time scale of approximately \( \pm 50 \) ns, so that we cannot make a precise measurement of any of the individual contributions. The goal of describing the peak structure mathematically is to obtain a function that can be used to estimate the total light intensity in the prompt region, and separate this contribution from effects with longer time constants.

The effective model for the prompt time structure consists of the sum of two gaussians:

\[
I_{\text{geo}}(t) = \nu_{\text{DET}} \cdot \text{Gaus}(t, \mu_{\text{DET}}, \sigma_{\text{DET}}) \\
+ \nu_{\text{DP}} \cdot \text{Gaus}(t, \mu_{\text{DP}}, \sigma_{\text{DP}}),
\]

with \( \nu_{\text{DP}} = 1 - \nu_{\text{DET}} \) and where \( \nu_{\text{DP}} \) is the probability for a pulse to arrive late, and \( \nu_{\text{DET}} \) in turn is the probability for a pulse to arrive at the nominal time.

Additionally, photoelectrons can skip a dynode in the PMT, leading to pulses that arrive early. This situation will be treated seperately later.

The PMTs also produce correlated noise, so-called afterpulsing (AP). AP in the DEAP-3600 PMTs occurs in three broad time regions centered at approximately \( 0.5 \) \( \mu \)s, \( 1.7 \) \( \mu \)s, and \( 6.3 \) \( \mu \)s. In the calibration of the PMTs, each of these regions is modelled using a gaussian distribution [35]. This simple model neglects small substructures within each AP region that are not relevant in analysis of single events, but become visible when looking at the summed pulseshape from many events. Nevertheless, we use the same model employed for PMT calibration here:

\[
I_{\text{AP}}(t) = \nu_{\text{AP}} \cdot \text{Gaus}(t, \mu_{\text{AP}}, \sigma_{\text{AP}})
\]

where \( i \) indicates the AP region, \( \nu_{\text{AP}} \) is the probability for an AP to occur in the respective region, \( \mu_{\text{AP}} \) is the time where the distribution is centered at, and \( \sigma_{\text{AP}} \) is its width.

We further consider AP of AP as the convolution of the AP distribution with itself:

\[
I_{\text{AP of AP}}(t) = I_{\text{AP}}(t) \otimes I_{\text{AP}}(t)
\]

AP of AP of AP is numerically insignificant and therefore not considered.

The random PMT noise (dark noise, DN) is modeled as a single constant term:

\[
I_{\text{DN}}(t) = r_{\text{DN}}
\]

This term contains the constant rate of qPE from sources not correlated with the event that triggered the detector; this includes the true thermionic PMT dark noise, the light level from radioactive decays in the PMT glass and surrounding material (causing for example low level Cherenkov light in the acrylic light guides), light from LAr events at such low energies that they do not trigger the detector and are not removed by pile-up cuts, and AP from all these effects.

4.4 Very late correlated light from previous events

Figure 2 shows that correlated light from \(^{39}\text{Ar}\) beta decay events is seen more than \( 18 \) \( \mu \)s after the event peak. Both the LAr triplet decay and PMT afterpulsing are well below dark noise level this late in the pulseshape. The observation is, however, what one expects if TPB has a very long-lived emission component: Each event selected in the energy windows discussed here is preceded by events that on average have a higher or much higher energy. The late TPB emission from these events will leak into following events, creating an average level of uncorrelated noise that is a function of the time since the previous event.

We use the term *stray light* to denote uncorrelated noise that includes both dark noise and the average residual light level from previous events. The stray light level is a function of the time that passed since the previous event. To measure the stray light level, we make use of the fact that each event’s trace starts 2.6 \( \mu \)s before the event peak. This pre-event window contains some of the light from previous events. We group all events by the time that passed since the previous event, \( \Delta t \). For each \( \Delta t \), we then determine the total light level in the pre-event window over all those events, \( N_{\text{p}}(\Delta t) \). The number of events in each group, \( N_{\text{ev}}(\Delta t) \) is also recorded. This allows us to map the stray light level as a function of the time since the previous even, \( I_{\text{stray}}(\Delta t) \), as

\[
I_{\text{stray}}(\Delta t) = \frac{N_{\text{p}}(\Delta t)}{N_{\text{ev}}(\Delta t)}
\]

In practice, a pre-event window of \( -1.6 \) \( \mu \)s to \( -1.0 \) \( \mu \)s is used, since the \( -2.6 \) \( \mu \)s to \( -1.6 \) \( \mu \)s region is used in one of the pile-up cuts; using an overlapping window would bias the measurement.
The result is converted to Hertz per PMT by dividing by the length of the sampling time window (0.6 µs) and the number of PMTs. Figure 3 shows this differential pre-event light rate for events of 200 µs digitization window, as well as for normal detector data recorded with a 16 µs digitization window.

![Fig. 3](image)

**Fig. 3** The pre-event light level as a function of $\Delta t$, for normal (16 µs) and long (200 µs) PMT trace data. Both the differential rate, and the average light level above the $\Delta t$ value (see text) are shown. In all cases, the curves approach a light level of approximately 142 Hz. The peaks at 20 µs and 200 µs are due to pile-up (see text).

When we make the average pulselshapes, we accept all events with $\Delta t \geq \Delta t_{cut}$, where $\Delta t_{cut}$ is either 20 µs or 200 µs, depending on the dataset. So we need the stray light level in an event when the previous event occurred at least $\Delta t$ before. This is obtained by determining the average stray light level above a given value of $\Delta t$:

$$T_{stray}(\Delta t) = \frac{\int_{\Delta t}^\infty N_p(\Delta t')d\Delta t'}{\int_{\Delta t}^\infty N_{cut}(\Delta t')d\Delta t'}$$

This distribution is called the weighted integral in Fig. 3, because $N_p(\Delta t)$ is implicitly weighted by the number of events at each $\Delta t$.

Finally, we assume that the pre-event light level obtained from events with $\Delta t \geq 21.6$ µs measures the stray light level at t=0 ns in events with $\Delta t \geq 20$ µs, and so on throughout the pulselshape. If $t$ is the time since the start of the event, that is the x-axis from Fig. 2, and $\Delta t$ is the time axis of Fig. 3, then the level of uncorrelated light at a given time $t$ in the event is $T_{stray}(\Delta t = \Delta t_{cut} + 1.6 \mu s + t)$.

The stray light level is highest near $\Delta t_{cut}$ due to pile-up in the preceding event. If $\Delta t$ was a perfectly accurate measure of the time difference to the last event, then we would not expect such a pronounced peak, and the curve for the long-digitization-window data would coincide with the curve for the normal data starting at $\Delta t=200$ µs. However, $\Delta t$ is calculated to the last trigger, and the DAQ does not re-trigger within the digitization window. Hence we have to differentiate between an event, that is an interaction that happens in the LAr and causes light emission, and a triggered event, that is an interaction that also causes the DAQ to trigger PMT read-out. If an event occurs within another event’s digitization window, the $\Delta t$ between triggers is larger than the actual time since the last event. The real $\Delta t$ can be as low as the time span that is the difference between $\Delta t_{cut}$ and the digitization window length. Since such a pile-up probability is constant in time, the uncorrelated light rate rises as the $\Delta t$ cut used approaches the length of the digitization window, regardless of the length of this window. The level it rises to is strongly influenced by the pile-up cut that removes events with too much light early in the trace.

We note that AP cannot cause the structures seen in Fig. 3 as it occurs at shorter time scales.

![Fig. 4](image)

**Fig. 4** The pre-event light level as a function of the $\Delta t$ cut, for a normal physics run (this is the same curve as in Fig. 3) and data taken with a $^{22}$Na gamma calibration source. The level of stray light increases due to the increased total event rate.

The pre-event pulse rate approaches the flat dark noise level at large values of $\Delta t$, i.e. it approaches $r_{DN}$ from Eq. (6). We use the $T_{stray}$ histograms to describe the time structure of all uncorrelated light and thus do not need $r_{DN}$ in the fit model.

The curves in Fig. 3 change with event rate and spectrum. To illustrate this, Fig. 4 shows a comparison between the stray light levels for normal physics data in a physics run (where the $^{39}$Ar provides the vast majority of events) to a run taken with a $^{22}$Na gamma calibration source. As expected, the rate of stray light increases, and it increases more strongly for values of $\Delta t$ near $\Delta t_{cut}$. Note that the source also induces an additional contribution to the flat dark noise level due to particles scattering on detector materials. Such scatters can cause Cherenkov photon emission, and reduce the energy of the particles as they reach the liquid argon, creating events with energy below the trigger threshold.
4.5 Full model

We describe the observed pulseshape by the convolution of detector effects with the LAr time structure. Detector effects in the prompt time region (−50 ns to 100 ns) are strongly degenerate in the fit. Therefore, we replace the decay parameter of the singlet component in the LAr PDF ($\tau_\text{LAr}$) with a generalized decay time $\tau_p$, which stands in for all the effects with exponentially falling time-structures at the ns scale.

$$I_{PS}(t) = \eta \cdot I_{\text{stray}}(\Delta T_{\text{cut}} + 1.6\,\mu s + t) + I_0 \cdot \left(I_{\text{LAr}}(t) \otimes I_{\text{TPB}}(t) \otimes I_{\text{geo}}(t) + I_{\text{LAr}}(t) \otimes [I_{\text{AP}}(t) + I_{\text{AP-stray}}(t)]\right)$$

(9)

where $\eta$ converts from Hz/PMT to pulse count.

AP following prompt photons creates a distinct peak in the pulseshape. AP in response to the LAr triplet decay is washed out but still creates a visible structure in the pulseshape. The TPB time structure is so extended that AP in response to it is washed out to the point where it is not visible in the pulseshape. Hence, AP in response to TPB delayed emission is not considered separately and the AP rate is absorbed in the overall TPB late emission probability.

A component due to early pulsing of the PMTs is added afterwards as $I_{EP}$. This component consists of the function $I_{PS}(t)$, shifted earlier in time and widened, since the early-pulsing has an intrinsic width. We model this by

$$I_{EP}(t) = I_0 \cdot R_{EP} \cdot \left(I_{\text{LAr}}(t - t_{\text{EP}}) \otimes I_{\text{TPB}}(t - t_{\text{EP}}) \otimes I'_{\text{geo}}(t - t_{\text{EP}})\right)$$

(10)

where in $I'_{\text{geo}}(t)$ the resolution of the gaussian is increased.

This component is not part of the fit, but is included when drawing the function:

$$I'_{PS}(t) = I_{EP}(t) + I_{PS}(t)$$

(11)

In practice, all terms contributing less than approximately 0.5% of the intensity at a given time are neglected in the evaluation of $I_{PS}$.

The model is constructed such that the total intensity $I_0$ is the only parameter that determines the overall amplitude. The intensity of all individual components is relative to this intensity. Since the AP probability in DEAP-3600 PMTs relatively large (approximately 8%), we re-calculate the intensities of the individual components after removing the AP contribution to the total intensity.

5 Pulseshape fits

We consider the pulseshape from events in the energy region of interest for WIMP search. The pulseshape has up to $10^7$ qPE per bin. With this many counts, the standard statistical uncertainty of the square root of the number of counts is dwarfed compared to systematic effects as small as 0.03% of the intensity in a bin. Since such small effects are not relevant when extracting information from the pulseshape or when simulating the detector response, they are not part of the model. Since the reduced $\chi^2$ is not a good indicator of goodness of fit in a situation where systematic errors dominate, we use the relative difference between the model and data instead of residuals to indicate how closely the model function describes the data. This quantity is shown below the figures in this section. The fit routine still attempts to minimize $\chi^2$; to improve convergence, the poissonian uncertainty in each bin is multiplied by a factor of 2, forcing $\chi^2$ to be smaller than it would be with standard uncertainties. The choice of multiplication factor has no significant effect on the extracted parameters. Due to $\chi^2$ not being a good statistical measure, parameter uncertainties from the fit will not be correct, and are therefore not quoted.

Many of the effects that influence the pulseshape are correlated, therefore it is not possible to obtain best fit values with high confidence for all parameters in the model. The goal of the fit is rather to obtain parameters such that the model describes the pulseshape well enough to be useful.

The parameters of the delayed TPB emission (Eq. (2)) are highly correlated with the LAr triplet decay time and with the AP rate. Therefore, we fix the TPB emission parameter values to those from [25] and only vary the total intensity of this component in the fit.

The AP rates and time structure (Eq. (4)) were calibrated in-situ before the DEAP-3600 detector was filled with LAr. However, AP rates can change with time and with PMT temperature. Two AP distributions at times of approximately 0.5 μs and 1.7 μs have a small probability and thus only a small effect on the pulseshapes. Their parameters are fixed by the calibration.

1 The fit parameters changed significantly between the arXiv version and the published version of this paper. The original arXiv version fit the TPB pulseshape from UV excitation fairly well out to 1 ms and included an intermediate term that captured some of the residual LAr intermediate component we use in this paper. The published version of the paper focuses the fit on earlier times and removes the dedicated intermediate component. It no longer fits the later part of the UV-light induced TPB pulseshape very well, which is the part of relevance for this work. Therefore, after communication with the authors of [25], the parameters we use here are those from the original arXiv version.
The AP distribution at approximately 6.6 µs dominates the pulseshape near that time, and the three parameters that describe it are varied in the fit to account for possible changes since the calibration.

The LAr triplet lifetime and the prompt lifetime (which accounts for the LAr and TPB prompt decay times, as well as the time structure from photons scattering in the detector) are varied in the fit.

The recombination time of the intermediate component is not constrained to the times quoted in [19], since the pulseshapes fit there are from interactions with protons or heavier nuclei, and we expect the shape to be different for low-energy electron-recoil events. The parameters that describe the prompt peak (Eq. 3) are all varied in the fit.

The shape of the stray light intensity is taken from Fig. 3 and \( \eta \) from Eq. 9 is adjusted such that the curves match the intensity of the pulseshape from \(-450\) ns to \(-200\) ns.

The fit is done in several stages, where parameters that dominate either the prompt (0 µs to 0.5 µs), the intermediate (0.5 µs to 8 µs), or the late (≥ 8 µs) region of the pulseshape are varied while all other parameters but the overall intensity and the singlet-to-triplet ratio are fixed in the fit. The set of parameters fit for one region is then fixed to its fit value when fitting the parameters for the next region. The prompt, intermediate, and late parameters are fit in turn and updated until the parameter values no longer change significantly. The early-pulsing component is added by manually adjusting the time difference, width, and early-pulsing probability to match the data at times before the peak. The prompt, intermediate, and late parameters were fit once more after adding this component.

The full fit region is \(-0.008\) µs to 160 µs. The initial estimates and the fit-out values for all model parameters are listed in Tab. 1 and 2, and a comparison between model and data is shown at three different time ranges in Figs. 5 through 7.

### Table 1 Start and fit parameters, LAr and TPB. Parameter uncertainties are not given, as explained in the text.

| LAr  |       |       |
|------|-------|-------|
| par  | start | fit   |
| \( R_p \) | 0.3   | 0.23  |
| \( \tau_p \) | 3 ns  | 8.2 ns |
| \( \tau_{rec} \) | -     | 75.5 ns |
| \( R_t \) | 0.7   | 0.71  |
| \( \tau_t \) | 1564 ns | 1445 ns |

| TPB  |       |       |
|------|-------|-------|
| par  | start | fit   |
| \( R_{TPB} \) | 0.06  | 0.1   |
| \( \tau_T \) | 20 \times 10^4 µs | -     |
| \( t_a \) | 12 µs | -     |
| \( A_{TPB} \) | 4.6   | -     |

The LAr triplet lifetime is strongly correlated in the fit with the TPB parameters \( A_{TPB} \) and \( t_a \), and with the afterpulsing probability in the 3rd afterpulsing region, \( \nu_{AP3} \). To investigate how much effect the TPB parameters have on the LAr triplet lifetime, we varied \( A_{TPB} \) and \( t_a \) each within \( \pm 2\sigma \) using the parameter uncertainties from [25]. For each combination of these parameter values, a fit was performed with all parameters fixed but for: \( \tau_1, \nu_{AP3}, R_s, R_t, R_{TPB} \), and the overall normalization \( I_0 \). The resulting parameter values are shown in Fig. 8 on a grid with the test values of \( t_a \) on the x-axis and the test values of \( A_{TPB} \) on the y-axis. The fit values for \( \tau_1, \nu_{AP3}, R_{TPB} \) are printed in each box, and the box is shaded by the ratio of the given fit’s \( \chi^2 \) to the value of \( \chi^2 \) from the nominal fit. While in this case, the reduced \( \chi^2 \) parameter cannot be used to infer a p-value, the relative difference for different model parameters is still a useful quantity saying something about how close the model comes to the data. The box

### Table 2 Start and fit parameters, instrumental effects. Parameter uncertainties are not given, as explained in the text.

| Detector |       |       |
|----------|-------|-------|
| par      | start | fit   |
| \( R_{det} \) | 0.97  | 0.985 |
| \( \mu_{det} \) | -1.8 ns | -     |
| \( \sigma_{det} \) | 5.1   | -     |
| \( \nu_{AP1} \) | 0.02  | -     |
| \( \sigma_{AP1} \) | 680 ns | -     |
| \( \nu_{AP2} \) | 0.055 | 0.068 |
| \( \sigma_{AP2} \) | 6300 ns | 6703 ns |
| \( \nu_{AP3} \) | 1.53  | 1.11  |
| \( \sigma_{AP3} \) | 1350 ns | 1229 ns |

### Fig. 5 At time scales beyond 15 µs, the pulseshape is dominated by the delayed TPB emission. At approximately 30 µs, the intensity of TPB emission has declined to the point where it is equal to the intensity of left-over late light from previous events.
this fit and the nominal fit is 1.2, but reaches this level before described by our LAr scintillation model. The time region so-called intermediate times (approx. 40 ns to 100 ns), is well spect to the event peak.

The prompt region of the pulseshape, including the LAr scintillation light. The region from 5 µs to 10 µs is dominated by PMT afterpulsing. Starting at approximately 13 µs, the TPB delayed emission becomes significant. While the total event length in standard DEAP data is 16 µs, the analysis window on which PSD as well as event energy and position reconstruction is based is −0.03 µs to 10 µs with respect to the event peak.

The triplet lifetime in this fit is 1435 ns. only if the late pulsing probability is allowed to vanish. The triplet lifetime in this fit is 1435 ns.

in the very center, outlined with a dashed line, is the nominal fit.

Fig. 9 shows the fit with nominal parameters, but the shape of the LAr intermediate component is changed to a simple exponential decay. The ratio of $\chi^2$ between this fit and the nominal fit is 1.2, but reaches this level

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig6}
\caption{From 0.2 µs to 5 µs, the pulseshape is dominated by the LAr scintillation light. The region from 5 µs to 10 µs is dominated by PMT afterpulsing. Starting at approximately 13 µs, the TPB delayed emission becomes significant. While the total event length in standard DEAP data is 16 µs, the analysis window on which PSD as well as event energy and position reconstruction is based is −0.03 µs to 10 µs with respect to the event peak.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig7}
\caption{The prompt region of the pulseshape, including the so-called intermediate times (approx. 40 ns to 100 ns), is well described by our LAr scintillation model. The time region before −8 ns is not part of the fit.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig8}
\caption{Each box corresponds to a fit where $A_{TPB}$ and $t_a$ are fixed to the value indicated on the axis. The box in the very center (light dashed outline) corresponds to the nominal fit where $A_{TPB}$ and $t_a$ are fixed to the best fit values from [25]. The values on the axes span the range from −$2\sigma$ to +$2\sigma$ using the parameter uncertainties from [25]. A measure for the typical relative difference between model and data is shown on the color scale (see text for an explanation of how this is calculated). The fit-out values for $\tau_c$ (in units of ns), $\tau_{AP3}$, and $R_{TPB}$ are printed in each box, in that order from top to bottom.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig9}
\caption{The prompt region of the pulseshape is shown again but the shape of the LAr intermediate is described as a single exponential decay.}
\end{figure}
The model described in Sect. 4 fits the observed pulselshape with deviations between model and data of less than 11% between 0 µs to 160 µs. The most significant deviation occurs in the time range of 15 µs to 50 µs. This time region is dominated by the delayed TPB emission, whose time-structure was described using the physics-based model and parameters from [25]. In [25], the TPB model does not describe the TPB pulselshape between 15 µs to 50 µs perfectly, either. Varying the model parameters within the uncertainties given, as shown in Fig. 8, lead to a slight improvement in the fit for some combinations, since the fit can compensate by changing the values of the free parameters. An alternate model for the delayed TPB emission is proposed in [20]. This effective model is based on a sum of exponential functions fit to the TPB emission pulselshape up to 10 µs, and fails to describe the pulselshapes discussed here for times $t \geq 10$ µs. We note that the delayed TPB emission may be subject to quenching by electronegative impurities such as oxygen. Therefore, the time structure measured in two experiments with different impurity profiles may differ.

The existence of delayed TPB emission means that each event contains light from previous events. For a 10 µs analysis window, approximately 3% of the total light intensity is emitted after the nominal end of the event. To be sure to analyze only events free from light belonging to previous events, event-time cuts of more than 200 µs must be chosen. With a background rate of 3300 Hz due to $^{39}$Ar decay in DEAP-3600, such a long event time cut removes too much livetime to be viable. The delayed light from previous events appears as time-variable uncorrelated noise in the analysis, in addition to the constant dark rate. We determined this stray light level by studying the light intensity in the pre-event window of each event as a function of the time difference to the previous event. The level depends strongly on the total event rate in the detector, the energy spectrum of events in the detector, and on the pile-up cuts used. The time profile for stray light found using this method under-estimates the observed light level in the pulselshape at late times by approximately 10%. This is likely due to subtle effects related to the trigger and data-quality cuts, since we compare the average pulse count very late in the pulselshape made from events selected by careful data-cleaning cuts to the average pulse count in the trace before the start of each event, with no control over what happened in the detector before the event. Particularly AP from light detected late in the previous event can increase the stray light rate as measured before the event peak.

The stray light component introduces subtle effects into the data. For example, given the dark noise rate of the PMTs, one would expect to measure on average 0.4 PE of uncorrelated noise in the 10 µs standard analysis window. Due to the long TPB decay component, the actual uncorrelated noise level is higher, and varies with the overall event rate and spectrum. In regular physics data, on average $(1.3 \pm 0.1)$ PE of uncorrelated noise are measured per event. The uncertainty accounts for the slight mismatch between the stray light model and the pulselshape data. During detector calibrations with radioactive sources, the energy spectrum is changed and the rate of events is increased, such that the uncorrelated noise level is higher. For the calibration with the $^{22}$Na source for example, it comes to 2.6 PE. This leads to systematic differences at the percent level in energy calibrations done with different types of calibration sources.

At low numbers of PE, PSD is also sensitive to the uncorrelated noise level. PSD in LAr is often based on the fraction of light detected in a prompt time window of $O(100$ ns$)$ around the event peak (FPrompt). Consider an event at 80 PE total, 30% of which occurs in the prompt window, so that the FPrompt parameter is 0.3. With 0.4 additional PE, of which, due to the length of the prompt and late windows, 10% occur in the prompt window and 90% in the late window, the measured FPrompt is 0.299. With 1.3 additional PE, the measured FPrompt value is 0.295 and with 2.6 additional PE, it is 0.290. A 1% to 3% energy-dependent shift in the value of the PSD parameter can result in a noticeable systematic effect in background leakage predictions.

The overall structure of the pulselshape between approximately 0.2 µs to 10 µs is well-described by the sum of the LAr triplet component, the TPB late time structure, and PMT AP. Periodic structures in the model-data comparison in the AP time regions are expected, since the AP time distribution has sub-features that the simple gaussian model from Eq. 4 does not capture. The 10% discrepancy at 12 µs falls at the intersection of the AP and AP-of-AP regions and might relate to subtleties in the AP-of-AP mechanism that are not modelled here.

The lifetime of the LAr triplet state we measure here is 1445 ns. The statistical uncertainty is negligible, however there are large systematic uncertainties: the LAr triplet lifetime is correlated with the parameters of the delayed TPB component, so the result is sensitive to whether or not this component is included in the analysis, and to the assumed time structure. As seen in Fig. 8, the triplet lifetime varies between 1387 ns to

\(^{2}\)The effect of instrumental biases on the Fprompt parameter is discussed in [11].
energy calibrations, and for particle identification through a detector. It has consequences for the interpretation of events and measured here for the first time in a large detector. The existence of delayed TPB emission has been proposed from dedicated small-scale setups and is verified with fine time-resolution and without the need for dedicated calibration data, due to the large rate of $^{39}$Ar $\beta$-decays available for analysis.

7 Conclusion

We present a complete model for the overall features of the pulleshape observed in a large LAr-based particle detector using TPB for wavelength shifting and PMTs for photon detection. The model accounts for the LAr intermediate component and delayed TPB emission. The model can also be used to understand detector behaviour by enabling a correct implementation of the signal shape in detector Monte Carlo simulation. The fits to the pulleshapes can be used to monitor instrumental effects, such as afterpulsing in PMTs, with fine time-resolution and without the need for dedicated calibration data, due to the large rate of $^{39}$Ar $\beta$-decays available for analysis.

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Several earlier measurements find smaller values near 1000 ns probably due to uncontrolled-for impurities in the LAr.

1544 ns when varying the delayed TPB emission parameters within their uncertainties. Removing the delayed TPB component from the fit, we measure a triplet lifetime of 1564 ns. Literature values range from 1300 ns to values near 1600 ns [16]. The measurement in [19] was done without the use of a wavelength shifter, while all the measurements that find values of 1500 ns or more use TPB and assume that TPB re-emits all photons within a few nanoseconds. We also note that the LAr triplet lifetime one infers is strongly dependent on the level and kind of impurities in the LAr [36,18,37,17,38].

Near the event peak, instrumental effects compound such that the value of $\tau_p$ given in Tab. 1 must be understood as a combination of the LAr singlet decay, TPB prompt emission, and scattering effects in the detector. We find that the model including a LAr intermediate component (19) described in Eq. 1 and surrounding text better describes our data than a simple exponential decay model. The hypothesis of delayed recombination could be tested by studying the pulleshape in a detector where an electric drift field can be applied. For a field high enough to drift all ionization electrons away from the interaction region, the intermediate component should disappear altogether.

If the hypothesis about delayed recombination is correct, the shape and intensity of the intermediate component should change with linear energy transfer. This would in principle offer another PSD-based handle on separating, for example, nuclear recoils from electron-recoil backgrounds. However, since this component does not dominate the pulleshape at any time, and only plays a role in a small time window, in practice, no PSD power improvement due to it should be expected. However, it should be taken into account when optimizing the length of the prompt window for Fprompt-like PSD parameters.
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