Sequence-dependent catalytic regulation of the SpoIIIE motor activity ensures directionality of DNA translocation

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Transport of cellular cargo by molecular motors requires directionality to ensure proper biological functioning. During sporulation in Bacillus subtilis, directionality of chromosome transport is mediated by the interaction between the membrane-bound DNA translocase SpoIIIE and specific octameric sequences (SRS). Whether SRS regulate directionality by recruiting and orienting SpoIIIE or by simply catalyzing its translocation activity is still unclear. By using atomic force microscopy and single-round fast kinetics translocation assays we determined the localization and dynamics of diffusing and translocating SpoIIIE complexes on DNA with or without SRS. Our findings combined with mathematical modelling revealed that SpoIIIE directionality is not regulated by protein recruitment to SRS but rather by a fine-tuned balance among the rates governing SpoIIIE-DNA interactions and the probability of starting translocation modulated by SRS. Additionally, we found that SpoIIIE can start translocation from non-specific DNA, providing an alternative active search mechanism for SRS located beyond the exploratory length defined by 1D diffusion. These findings are relevant in vivo in the context of chromosome transport through an open channel, where SpoIIIE can rapidly explore DNA while directionality is modulated by the probability of translocation initiation upon interaction with SRS versus non-specific DNA.

Bacterial DNA pumps are responsible for the intra and intercellular transfer of genetic material across membranes during sporulation, cell division and conjugation. SpoIIIE is responsible for the directional translocation of double-stranded DNA during sporulation and cell division in Bacillus subtilis (B. subtilis)2–6. SpoIIIE is composed of an N-terminal transmembrane domain involved in septal localization4, an unstructured linker and a C-terminal motor domain that assembles as a hexameric ring5. The cytoplasmic motor domain of SpoIIIE can be subdivided into three separate subdomains: the α and β subdomains that contain the core ATPase machinery ensuring DNA translocation and the γ subdomain that recognizes a tandem of 8 base pair repeats (termed SRS for SpoIIIE Recognition Sequence) in an orientation-specific manner6. Similarly to other Rec-A like NTPases, SpoIIIE preferentially tracks the 5′ → 3′ strand in the direction of translocation8,9.

The detailed molecular mechanism by which SRS regulates motor directionality is still a matter of debate. It has been shown that SpoIIIE has higher affinity for SRS than for non-specific DNA and that SRS stimulates its ATPase activity11,12, suggesting that SRS could either regulate directionality by recruiting and orienting SpoIIIE hexamers prior to engaging translocation or by simply triggering SpoIIIE translocation. Predictions based solely on ATPase measurements were recently challenged by a study showing that SpoIIIE ATPase and translocation activities can be decoupled by mutating specific residues13. Hence, the distinction between these two mechanisms (recruitment and orienting vs. catalytic triggering) requires direct observation of SpoIIIE-DNA complexes and discrimination between the translocating state when complexes are interacting with non-specific DNA or with SRS.

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Here, we study how sequence recognition regulates the directionality and translocation activity of SpoIIIE by combining single molecule imaging with single round translocation measurements and mathematical modelling. We directly observed and quantified the number of diffusing and translocating complexes on DNA with and without SRS by atomic force microscopy (AFM) and further analyzed their dynamics by single-round translocation kinetics measurements (triplex displacement assay). To interpret our experimental results, we developed a mathematical model accounting for all the biochemical processes describing the interaction between SpoIIIE and DNA (i.e., association, dissociation, 1D diffusion, ATP activation and translocation). We show that, in contrast to predictions from previous models 12, SpoIIIE can actively translocate on DNA independently of the presence of specific sequences, and that SRS modulates the translocation activity of SpoIIIE. Our results strongly suggest that rather than recruiting and orienting the non-active protein, SRS sequences regulate directionality by modulating the translocation activity of SpoIIIE.

Results

SpoIIIE can efficiently couple ATP hydrolysis to translocation independently of the presence of SRS sequences. Different studies agree that SpoIIIE activity is stimulated by SRS 12, however the capacity of SpoIIIE to efficiently couple ATP hydrolysis to translocation in absence of SRS remains unclear. Based on ATPase activity measurements, it has been proposed that SpoIIIE activity is inhibited in absence of SRS sequences 12. However, biochemical and single molecule studies reported the capacity of SpoIIIE to hydrolyze ATP and to translocate when interacting with non-specific DNA 6,11. ATPase activity of the motor allows to infer translocation, but may not be a definitive proof as the enzyme could be performing futile cycles of ATP hydrolysis (i.e. not converting the chemical energy into mechanical movement) or ATP hydrolysis may go undetected depending on the methodology employed. On the other hand, single molecule studies do not allow to simultaneously quantify ATP hydrolysis and translocation to conclude unambiguously on the efficiency of the mechanochemical transduction. To directly test the ability of SpoIIIE to couple ATP hydrolysis to translocation independently of the presence of SRS, we performed AFM imaging of SpoIIIE incubated with linearized DNA substrates without or with SRS sequences oriented towards the nearest DNA end (DNA_{SRS} and DNA_{NS}, respectively) in the presence and absence of ATP. First we sought to evaluate the capacity of SpoIIIE to hydrolyze ATP when incubated with either substrate. Interestingly, SpoIIIE displayed equivalent specific ATPase activity in both DNA_{SRS} and DNA_{NS} (Fig. S1E). When evaluating spatial localization of SpoIIIE in DNA, in absence of ATP 38% of the detected SpoIIIE was bound to SRS in DNA_{SRS} (Figs 1A,C and S1A) whereas less than 10% of SpoIIIE located to the equivalent position in DNA_{NS} (Figs 1B,C and S1B). Strikingly, when adding ATP SpoIIIE preferentially localized at the DNA ends (~40%) independently of the presence of SRS (Figs 1D–F and S1C,D). These results indicate that SpoIIIE can explore the DNA without using the energy provided by ATP hydrolysis to reach SRS while becoming activated and translocating DNA with similar efficiencies independently of the presence of SRS.

Figure 1. SpoIIIE can actively translocate and reach DNA ends even in the absence of SRS sequences. (A,B) AFM micrographs of SpoIIIE bound to SRS (DNA_{SRS}) and to non-specific DNA (DNA_{NS}) in the absence of ATP. Arrows indicate SpoIIIE complexes bound to SRS (green arrow in panel A) and to equivalent position replaced by non-specific DNA as a control (orange arrow in panel B). (C) Relative frequency of SpoIIIE binding to SRS (DNA_{SRS}) or to the equivalent position replaced by non-specific DNA (DNA_{NS}, control). The position of SpoIIIE complexes in DNA was determined using a semi-automated algorithm and the relative frequency of SpoIIIE localization in bins of 50 nm was calculated (see Fig. S1A,B, Material and Methods and Supplementary Information). Error bars were obtained from the error propagation of Eq. 1 (n = 35). Upper scheme represents SpoIIIE bound to SRS and to the equivalent position replaced by non-specific DNA. (D,E) AFM micrographs of SpoIIIE complexes with DNA_{SRS} and DNA_{NS} substrates in the presence of ATP. Red arrows indicate SpoIIIE complexes that have reached the DNA ends by translocation. (F) Relative frequency of SpoIIIE reaching DNA ends by translocation in substrates with (DNA_{SRS}) or without (DNA_{NS}) SRS. The position of SpoIIIE complexes in DNA was determined as described in panel C (see Fig. S1C,D, n = 40). Upper scheme represents SpoIIIE reaching the DNA ends for substrates with or without SRS. Relative frequencies depicted in panel C were recalculated from previously published data 11.
To further understand the interaction of SpoIIIE with SRS and non-specific DNA as well as the regulation of its translocation activity, a mathematical model describing the binding and diffusing properties of SpoIIIE was extended to include DNA translocation. The model mimics the two experimental scenarios for DNA with or without SRS sequences (Fig. 2A,B). Briefly, SpoIIIE is able to interact non-deterministically with SRS and non-specific DNA sequences with distinct association and dissociation probabilities per time step $p_{on}^{SRS}$, $p_{off}^{SRS}$, $p_{on}^{NS}$, and $p_{off}^{NS}$. When bound to DNA, SpoIIIE can undergo 1D diffusion defined by the sliding length $sld$. In the presence of ATP, SpoIIIE can become active with a probability $p_{ATP}$ and translocate at constant velocity $v_{trans}$. Probabilities of binding, unbinding, sliding lengths and activation by ATP could be set to distinct values depending on the DNA substrate. When the triplex was present, translocating SpoIIIE can displace the triplex when reaching the corresponding DNA end with probability $p_{triplex}$. See Material and Methods and Supplementary Information for additional details.

Figure 2. Scheme of the mathematical model encoding the dynamics of SpoIIIE/DNA interaction. (A,B) In the model SpoIIIE can interact with non-specific DNA (DNA_{NS}, A) and SRS containing DNA (DNA_{SRS}, B). The dynamics of non-active SpoIIIE (i) were modelled as a Markov process controlled by the SpoIIIE binding/unbinding probabilities ($p_{on}/p_{off}$) to/from non-specific or SRS regions of DNA (orange and green solid lines respectively). Once bound to DNA, SpoIIIE can undergo 1D diffusion defined by the sliding length $sld$. In the presence of ATP (ii), SpoIIIE can become active with a probability $p_{ATP}$ and translocate at constant velocity ($v_{trans}$). Probabilities of binding, unbinding, sliding lengths and activation by ATP could be set to distinct values depending on the DNA substrate. When the triplex was present (iii), translocating SpoIIIE can displace the triplex when reaching the corresponding DNA end with probability $p_{triplex}$. See Material and Methods and Supplementary Information for additional details.

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First, we assessed the model in the absence of translocation and evaluated the relative frequency of SpoIIIE binding to SRS. Experimentally it has been shown that SpoIIIE associates with identical rates to SRS and non-specific DNA, whereas dissociation from SRS is ~3 times slower. The model parameters were set to values emulating these experimental binding rates and different sliding lengths of SpoIIIE when interacting with non-specific DNA or SRS were explored (Fig. S2). AFM distributions for DNA_{SRS} were recovered when SpoIIIE explored large regions of non-specific DNA ($sld^{NS}=145$ bp) whereas it was almost immobile when bound to SRS ($sld^{SRS}=1$ bp, Fig. 3A upper panel and S2 and Movie M1). Equivalent results were obtained when employing anomalous 3D hopping as DNA exploring mechanism (unpublished data). To evaluate the robustness of the model, the binding and diffusion parameters were varied at least one order of magnitude above and below the optimal values (Fig. 3B,C and Table 1). When 1D diffusion was absent or equivalent between non-specific DNA and SRS, experimental distributions were not recovered for the large majority of the parameter values (Fig. 3B,C, see Fig. S2 for discussion of these results). Detailed observation of single molecule trajectories revealed that SpoIIIE either did not remain bound to SRS or the frequency of interaction with SRS by direct binding was extremely low in this conditions (Fig. 3A middle and lower panels respectively). When the ratio $sld^{NS}/sld^{SRS}$ was set at 145, the model reproduced the AFM obtained distributions for a large set of association probabilities, whereas in similar conditions only a narrow set of dissociation probabilities values reproduced the localization
of SpoIIIE to SRS (Fig. 3B,C). These results indicate the critical role of anomalous diffusion (sld_{NS} >> sld_{SRS}) and SRS dissociation rate (p_{off_{SRS}} < p_{off_{NS}}) in regulating DNA exploration and stable binding to ensure SRS recognition.

Next, we evaluated the localization of SpoIIIE when incubated with DNA_{SRS} and DNA_{NS} in the presence of ATP and quantified the relative frequency of proteins reaching the DNA ends. First, using the previously validated parameter values (Figs 3B,C and S2 and Table 1), we tested the simplest case in which all proteins became instantly active after binding to DNA (p_{ATP} = 1) for a large range of translocating velocities. Under these parametric settings proteins do not explore DNA by 1D diffusion (Fig. 4A lower panel) and simulations showed that the relative number of SpoIIIE located at the DNA ends hyperbolically increased with translocation velocities to values largely exceeding AFM observations for both DNA_{NS} and DNA_{SRS} (Fig. 4B). Notably, the translocation velocities reproducing experimental SpoIIIE distributions on DNA were below 0.1 kb.s^{-1} (Fig. 4B), a value far below the reported translocation velocities in equivalent experimental conditions (4 to 7 kb.s^{-1} at 20 °C). We reasoned that the model did not reproduce experimental DNA distributions of SpoIIIE due to the extreme conditions imposed: instantaneous activation of DNA-bound motors is biologically unlikely. When reducing the probability of activation by ATP, SpoIIIE was able to randomly bind, explore large regions of non-specific DNA

Table 1. Model parameters values satisfying experimental results.
Figure 4. Model predicted dynamics and distributions of SpoIIIE in DNA_{SRS} and DNA_{NS} in the presence of ATP. (A) Representative trajectories of SpoIIIE when interacting with DNA_{SRS} in the presence of ATP. Each panel represents a DNA molecule where the activation probability \( p_{ATP} \) and translocating velocity \( v_{trans} \) were varied with values shown on the right of each panel. The rest of the parameters were set at the values depicted in Table 1. Horizontal and vertical axis represent time evolution in Monte Carlo steps (MCS) and DNA coordinates (in base pairs, bp), respectively. Color code from Fig. 3A is conserved and translocating proteins are depicted in red. Translocation velocity was reduced 10 times with respect to the value depicted on the right solely for representation purposes. Scheme on the right depicts non-specific DNA regions (solid black line) and SRS sites (semi-transparent green triangles). (B, C) Model-predicted relative frequency of SpoIIIE reaching DNA ends for DNA_{SRS} (green squares) and DNA_{NS} (orange circles) as a function of translocation velocity with ATP activation probability \( p_{ATP} = 1 \) (B) and as a function of \( p_{ATP} \) for different translocation velocities (C). Solid lines connecting dots are only a guide to the eye. Orange and green dashed lines and grey shadow area indicate the experimental mean relative frequency and standard deviation respectively for both substrates in the presence of ATP. All other parameter values were set at the values depicted in Table 1. Upper scheme represents SpoIIIE reaching the DNA ends for substrates with or without SRS.

SpoIIIE translocation directionality is catalytically regulated by SRS. To assess if protein translocation activity is regulated by SRS, we implemented a fast kinetics assay with temporal resolution on the seconds scale that allows for monitoring single-round cycles of the enzyme arrival at the DNA end proximal to SRS. The substrates were identical to those employed for AFM measurements but contained a fluorescently labelled triplex-forming oligonucleotide inserted at the 5' end (Fig. 5A). Displacement of triplex by SpoIIIE was monitored in real time by following the changes in fluorescence anisotropy of the TAMRA-labelled triplex (Fig. 5A,B). In presence of SpoIIIE but no nucleotide, triplex anisotropy was constant for more than 25 minutes (Fig. 5B inset), indicating that the triplex was stably bound and that diffusing SpoIIIE did not displace them. In contrast, in the presence of ATP and SpoIIIE, the triplex anisotropy rapidly decreased with time (Fig. 5B), indicating that ATP-fueled DNA translocation by SpoIIIE leads to triplex displacement. Interestingly, the kinetics of triplex displacement by SpoIIIE were faster in the substrates containing SRS (Fig. 5B). The differences in kinetics between...
substrates was quantified from the ratio between the areas under the kinetic traces for DNA_SRS and DNA_NS (θ_{SRS/NS} = 0.62 ± 0.06), and showed that SRS accelerates by ~60% the triplex displacement rate. In vivo and in vitro SpoIIIE is capable of removing from DNA tightly bound complexes such as RNA polymerase and transcription factors17. Moreover additional simulations confirmed the capacity of SpoIIIE to reach DNA ends of both substrates in equivalent manner independently of the presence of the triplex (Fig. S6). Thus, the observed differences in the displacement rates should arise from changes in the intrinsic activity of SpoIIIE.

To evaluate the mechanism responsible for accelerated triplex displacement in DNA_{SRS}, the model was extended to include a triplex at the 5' DNA end (Fig. 2A–Biii). Kinetic traces in the presence and absence of SRS were simulated and the ratio of the area under the curves (θ_{SRS/NS}) was calculated as for the experimental

**Figure 5.** SRS enhances ATP-dependent translocation activity of SpoIIIE. (A) Scheme representing the triplex displacement experimental design. (B) Time course of triplex displacement by SpoIIIE for substrates with (green circles) or without (orange squares) SRS sequences in the presence of ATP. Inset shows that in the absence of ATP, SpoIIIE is unable to displace the triplex. (C) Effect of SRS in triplex displacement rates quantified as the ratio between the area under the kinetic traces for DNA_{SRS} and DNA_{NS} (θ_{SRS/NS}). Blue squares and error bars indicate mean and standard deviation from the simulation results by varying p_{ATP}^{SRS} while maintaining p_{ATP}^{NS} constant at 0.012. Red circle depicts the result expected for the 'recruitment and orient' directionality model (see main text). Green dotted line and grey shaded area indicate the mean and standard deviation of θ_{SRS/NS} obtained from the experimental results shown in panel B (n = 3). Solid blue lines connecting squares are only a guide to the eye. Insets depict the time courses for triplex displacement obtained from simulations when p_{ATP}^{SRS} = p_{ATP}^{NS} (left) and p_{ATP}^{SRS} = 0.8 (right). Parameter values for simulations are depicted in Table 1. (D) SpoIIIE in vivo directionality mechanism. Free, bound, diffusing and active SpoIIIE are represented in grey, black, dotted grey and filled light blue respectively. Dotted green and orange contour lines represent the two alternative pathways for SpoIIIE directionality regulation. Upon binding (black arrow) SpoIIIE can explore DNA by diffusion (dotted grey arrow) and/or dissociate (red arrows) and/or become active (green arrows). Once active SpoIIIE can translocate (dashed black arrows). Thickness of red and green arrows is proportional to the rate/probability values obtained from experimental and modelling optimized parameter values when SpoIIIE is interacting with non-specific or SRS sequences. Upper scheme depicts a B. subtilis cell in the initial stages of sporulation. oriC regions (red circles) move towards the cell poles and after asymmetric division SpoIIIE (blue circles) is recruited to the septum to transport two-thirds of the chromosome into the forespore.
conditions. Initially, the optimal parameter values obtained in the previous section were employed ($v_{\text{trans}} = 5 \text{ kb s}^{-1}$ and $p_{\text{ATP}} = 0.012$, see Table 1). In these conditions, the rates of triplex displacements for substrates with or without SRS were almost equivalent ($\theta_{\text{SRS/NS}} = 0.95 \pm 0.06$, Fig. 5C left inset), indicating that the higher affinity of SpoIIIE for SRS is not enough to explain the faster rate of displacement in the presence of SRS. To further test if protein orientation by SRS is an essential element of the directionality regulation, the directionality parameter ($p_{\text{dir}}$) was varied to modulate the probability of SpoIIIE to translocate in a given direction when activated by SRS. When setting the probability of translocating towards the triplex to a 100%, the model was still unable to reproduce the acceleration observed in triplex displacement when SRS is present ($\theta_{\text{SRS/NS}} = 0.74 \pm 0.02$, Fig. 5C red dot). These results indicate that the recruitment of SpoIIIE to SRS and the polarization in the direction of translocation imposed by the specific sequences do not suffice to efficiently regulate the motor directionality.

To test whether stimulation of SpoIIIE motor activity by SRS could be responsible for the faster triplex displacement rate, we explored different values for $p_{\text{ATP}}$, where $p_{\text{ATP}}^{\text{SRS}} = p_{\text{ATP}}^{\text{NS}}$. When increasing the $p_{\text{ATP}}^{\text{SRS}}/p_{\text{ATP}}^{\text{NS}}$ ratio (while fixing $p_{\text{ATP}}^{\text{NS}} = 0.012$), $\theta_{\text{SRS/NS}}$ decreased non-linearly reaching the experimental range when $p_{\text{ATP}}^{\text{SRS}} > 0.4$ (Fig. 5C). Indeed, values of $p_{\text{ATP}}^{\text{SRS}}$ above 0.4 did not further increase the triplex displacement rate, indicating that the number of proteins getting to SRS becomes eventually limited by the ATP-independent steps of the biochemical cycle of translocation (i.e., association, dissociation and diffusion). When using an equivalent probability ($p_{\text{dir}}$) for SpoIIIE to translocate in any direction the model can satisfactorily reproduce the experimental results fulfilling the parsimony principle and revealing the central role of catalytic regulation of SpoIIIE by SRS in directionality regulation. Next, we sought to evaluate if coupling activation by SRS with orientation regulation could improve the model capacity to reproduce the SpoIIIE dynamics. Thus, we set the directionality parameter described previously to modulate the orientation of SpoIIIE with an intermediate efficiency (70% of recognition) and with 100% as control. The values of $p_{\text{ATP}}^{\text{SRS}}$ were lower than when no directionality was imposed, while the overall quality of the fittings remained comparable to the case in which no directionality bias was imposed by SRS. Interestingly, we observe that there is a very limited range of probabilities of activation by SRS in which the model could reproduce the experimental curves when the directionality parameter was introduced (Fig. S7). Thus, according to our modelling results, translocation directionality would not be regulated by the higher affinity of SpoIIIE for SRS but rather by the higher probability of activation of the ATP-fueled translocation activity of SpoIIIE upon encountering SRS. Favoring the activation of SpoIIIE whose orientation matches that of SRS or that are re-oriented by SRS may contribute to the directionality mechanism, but faithful achievement of correct directionality requires in all cases the motor activity modulation by SRS.

Discussion
In this study, we investigated the detailed mechanisms by which SRS sequences regulate the SpoIIIE motor directionality by combining single-molecule imaging and fast kinetics translocation assays with mathematical modeling. Current models agree that specific sequences determine SpoIIIE directionality according to their orientation and that SpoIIIE ATPase activity and affinity are higher when SRS are present on DNA. However, it remained unclear if these sequences are necessary or sufficient to trigger motor translocation and whether this is the main mechanism by which they regulate directionality.

The capacity of non-specific DNA to trigger the translocation activity of the SpoIIIE motor is a major source of discrepancy between previously proposed models for directionality regulation. Our strategy employing atomic force microscopy imaging allowed the direct observation of SpoIIIE complexes after full translocation cycles on linearized DNA. This finding was further confirmed by fast kinetics translocation assays with mathematical modeling. Current models agree that specific sequences determine SpoIIIE directionality according to their orientation and with 100% as control. The values of $p_{\text{ATP}}^{\text{SRS}}$ were lower than when no directionality was imposed, while the overall quality of the fittings remained comparable to the case in which no directionality bias was imposed by SRS. Interestingly, we observe that there is a very limited range of probabilities of activation by SRS in which the model could reproduce the experimental curves when the directionality parameter was introduced (Fig. S7). Thus, according to our modelling results, translocation directionality would not be regulated by the higher affinity of SpoIIIE for SRS but rather by the higher probability of activation of the ATP-fueled translocation activity of SpoIIIE upon encountering SRS. Favoring the activation of SpoIIIE whose orientation matches that of SRS or that are re-oriented by SRS may contribute to the directionality mechanism, but faithful achievement of correct directionality requires in all cases the motor activity modulation by SRS.

To discriminate between the two mechanisms, we expanded the mathematical model to reproduce the experimental triplex displacement traces. Simulations showed that the higher affinity of SpoIIIE for SRS coupled with 100% efficiency in protein orientation can not reproduce the translocation dynamics of SpoIIIE, strongly suggesting that directionality is not regulated by SpoIIIE being recruited and oriented by SRS. On the contrary, when SRS was allowed to modulate the translocation activity of SpoIIIE, the simulations recovered the experimentally observed kinetics when the probability of activation by SRS was ~30 times higher that by non-specific DNA. Then, combined with the lower dissociation probability from SRS ($p_{\text{off}}^{\text{SRS}}/p_{\text{off}}^{\text{NS}} \approx 2.3$), our model predicts that SpoIIIE is ~70 times more likely to start translocating when bound to SRS than to non-specific DNA. Adding
protein orientation by SRS improves the efficiency of the directionality regulation mechanism and allows to reach equivalent effects with lower probabilities of activation by SRS, but still this activation probabilities remain at least 10 times higher than when SpoIIIE is interacting with non-specific DNA. Altogether, our experimental and modeling results contrast with directionality regulation models proposed for SpoIIIE and its homologue FtsK12,19 while proving that SRS sequences do not only increase the ATPase activity of SpoIIIE as it has been previously shown1,12, but also have a determinant effect in the initiation of DNA translocation.

Rather than SpoIIIE being recruited and re-oriented by SRS, the mechanism defining directionality is exclusively dependent on the capacity of SRS to modulate the activation and translocation of SpoIIIE. Additionally the randomly occurring match between SRS and SpoIIIE orientation could fine tune or reinforce synergistically the SRS triggering action to safeguard translocation start in a non-favorable direction during sporulation. This in vitro observations can indeed account for the in vivo behavior of SpoIIIE if transport of DNA was occurring through a preexisting DNA-conducting pore before the final closure of the septum as it has been proposed previously21,22. As in the in vivo context the concentration of ATP will not be rate limiting in the protein catalytic cycle; this mechanism may have evolved to an optimal where directionality regulation relies on a rapid local search by 1D diffusion to bind stably to SRS and a robust catalytic modulation of the enzyme translocation activity if orientations match (Fig. 5D, ‘Polarity match pathway’).

Future in vivo studies with high spatial and temporal resolution should hold the key to further test the new directionality regulation model proposed in this work.

Materials and Methods
SpoIIIE purification and activity. SpoIIIE was expressed and purified as described previously6. ATPase measurements were performed in identical buffer and temperature conditions to those employed for incubation of the protein prior to AFM imaging and triplex displacement measurements with the addition of reagents from EnzCheck Pyrophosphate Assay Kit (Molecular Probes, USA). ATPase activity was measured as the initial velocity of release of Pi from ATP. Protein concentration was in all cases ~10 nM monomer. At this concentration from EnzCheck Pyrophosphate Assay Kit (Molecular Probes, USA) SpoIIIE is mostly in hexameric state11 ensuring a stoichiometry of ~1 hexamer per DNA molecule.

DNA substrates. DNA substrates were assembled by cloning duplex oligos containing 3-mer repeats of SRS (GAGAAGGGAGGAGGAGGAGG) or a random sequence replacing the SRS with equivalent CG content (GGGCGCGGGCGGGCGGGCGCG) into the SpeI site of a derivative of the pBS SK(+) and the final products were verified by sequencing as described previously (Levy et al. 2005).

AFM imaging and quantification. Mica (Goodfellow, France) was freshly cleaved and 1 μl of a 1 mM NiCl2 was deposited, incubated for 1 min and rinsed with 1 ml of deionized water (Millipore, Germany). Samples (2 nM DNA + 15 nM protein) were mixed and incubated for 2 minutes before deposition into the mica. Samples were deposited for 2 min and next rinsed with 3 ml of deionized water, dried with nitrogen and kept in a desiccator until imaging. AFM Images were obtained with a Nanoscope IIIa microscope (Veeco, France) equipped with a type-E scanner and operating in tapping mode in air using AC160 TS Olympus cantilevers (Olympus Corporation, Japan) as described23.

Image analysis was carried out using MATLAB (MathWorks, USA) and distributions of the localization of proteins on DNA were represented as relative frequency histograms with bin sizes of 50 nm. The relative frequency of SpoIIIE at SRS or DNA ends (F) was quantified as the ratio between the number of SpoIIIE located at the first bin f(x₁) and the total number of proteins bound to DNA ∑ₙ₌₁ⁿ⁻¹f(xᵢ):

\[ F = \frac{f(x₁)}{\sum_{i=1}^{n-1} f(x_i)} \]  

(1)

The absolute error of the relative frequency estimation for the first bin displayed in Fig. 1C and F was calculated from the error propagation of Eq. 1 assuming an uncertainty of ±1 SpoIIIE proteins per bin.

A detailed description of image analysis procedure and quantification is given in the Supplementary Information section.

Triplex displacement assays. Fluorescent triplex substrates were prepared as described previously6 by using the same DNA substrates as for AFM imaging and a triplex forming oligonucleotide bearing a 5’-TAMRA fluorophore (Euorgenetec, Belgium). Triplex displacement reactions were conducted at 27 °C following fluorescence anisotropy (FA) changes using a microplate reader, (excitation set to 530 nm and emission measured at 580 nm). 30 μL of 10 nM SpoIIIE was rapidly mixed with 30 μL of DNA-Triplex (1.2 nM) and FA signal was followed over time with a time resolution of ~7 s and a dead time of 15 s.

Mathematical model encoding for SpoIIIE/DNA interactions. SpoIIIE-DNA dynamics were studied by means of a combined deterministic/non-deterministic mathematical model in which m DNA molecules were represented as single arrays containing n sites to which r SpoIIIE proteins can bind/unbind with probabilities p⁺off/ p⁻off, respectively (Fig. 2). Bound SpoIIIE can unbind or slide (1D diffusion) along the DNA to another site a sliding distance sld, ± sld (mean ± sd, in base pairs). All interactions not involving ATP-dependent mechanisms were modelled as a Markov process. In the presence of ATP, DNA-bound SpoIIIE can start translocating with a probability pATP. When interacting with SRS SpoIIIE translocation direction is set with a probability pdir. Depending on the substrates characteristics (i.e., with or without SRS) SpoIIIE can interact with nSRS or nNS sites with distinct probabilities for all the previously described processes.
Once activated, SpoIIIE can randomly translocate in either direction. Translocation was deterministically modeled as a movement along the DNA with uniform velocity $v_{\text{trans}}$. For the sake of simplicity, it is assumed that during translocation, SpoIIIE can dissociate from DNA with probability $p_{\text{off}}$ for all types of sites. In case of collision between two SpoIIIE molecules only one will remain bound with translocating complexes taking priority over bound or diffusing SpoIIIE. When reaching the DNA end (by 1D diffusion or translocation), SpoIIIE protein stops and can dissociate with a probability $p_{\text{off}}$ or diffuse back to another site, reflecting on the boundaries. The relative frequency of SpoIIIE bound to SRS in the absence of ATP (for DNA$_{\text{NS}}$) was calculated as the temporal average of the ratio between the total number of proteins bound to SRS and the total number of proteins bound the DNA substrate. In the presence of ATP, the relative frequency of SpoIIIE arriving at the DNA ends (for DNA$_{\text{NS}}$ and DNA$_{\text{poff}}$) was calculated as the temporal average of the ratio between the number of SpoIIIE reaching both DNA ends positions and the total number of proteins bound to the DNA substrate. In all the cases, the temporal averages were calculated over the last 1,000 MCS (see Supplementary Information).

To simulate the triplex displacement kinetics, the presence of a triplex forming oligonucleotide on the DNA end next to the SRS sequence (which is replaced by non-specific base pairs in the DNA$_{\text{NS}}$ substrates) was added. When SpoIIIE, by translocation, arrives to the DNA end, it releases the triplex with probability $p_{\text{triplax}} = 1$ and this DNA molecule is no longer considered during the remainder of the simulation. To quantitatively compare the simulation results to experimental data it was assumed that the accumulated number of released triplex in the simulations is linearly proportional to a theoretical anisotropy signal and the ratio between the area under the curves of kinetic traces for DNA$_{\text{NS}}$ and DNA$_{\text{tripl}}$ was calculated (see Supplementary Information). Additional model details, parameterization and quantification are given in the Supplementary Information.

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Author Contributions
D.I.C. and M.N. conceived and designed the experiments. D.I.C. and P.E.M. performed the experiments. O.C., M.N. and D.I.C. conceived the mathematical models. O.C. developed the mathematical models and software. O.C. and A.B. implemented the software. O.C. and D.I.C. analyzed the data. O.C., M.N. and D.I.C. wrote the manuscript.

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