PINGU:
A Vision for Neutrino and Particle Physics at the South Pole

M. G. Aartsenb, K. Abrahamak, M. Ackermannbg, J. Adamsp, J. A. Aguilarj,
M. Ahlersae, M. Ahrensav, D. Altmannx, K. Andeenah, T. Andersonbc, I. Anseauj,
G. Antonx, M. Archingeraf, C. Arguellesa, T. C. Arlenbc, J. Auffenberga, S. Axani,
X. Baiat, I. Bartosas, S. W. Barwickaa, V. Baumaf, R. Bayg, J. J. Beattyrs,
J. Becker Tjusl, K.-H. Becketlb, S. BenZvirbd, P. Berghausaji, D. Berleyq, E. Bernardinibg,
A. Bernhardak, D. Z. Bessonah, G. Binderh, D. Bindigbf, M. Bissokx, E. Blaufussq,
S. Blotbg, D. J. Boersmabe, C. Bohmav, M. Börneru, F. Bosj, D. Boseax, S. Böseraf,
O. Botnerbe, J. Braunae, L. Brayeurm, H.-P. Bretzbg, A. Burgmanbe, T. Carverv,
M. Casierm, E. Cheunga, D. Chirkine, A. Christovx, K. Clarkaz, L. Classenn,
S. Coendersak, G. H. Collinn, J. M. Conradn, D. F. Cowenc, R. Crossbd, M. Dayae,
J. P. A. M. de Andrév, C. De Clercqm, E. del Pino Rosendoa, H. Dembinskin,
S. De Ridderx, P. Desiatiæ, K. D. de Vriesm, G. de Wasseigem, M. de Withl,
T. DeYoungv, J. C. Díaz-Vélezæ, V. di Lorenzoã, H. Dujmovicax, J. P. Dummav,
M. Dunkmanbc, B. Eberhardtæ, T. Ehrhardtæ, B. Eichmannj, P. Ellerbc, S. Eulerbe,
J. J. Evansæ, D. P. Evensonæ, S. Faheyæ, A. R. Fazelyf, J. Feintzeigæ, J. Feldoa,
K. Filimonovã, C. Finleyæ, S. Flisæ, C.-C. Fösiga, A. Franckowiakbg, E. Friedmanq,
T. Fuchsæ, T. K. Gaisseræ, J. Gallagheræ, L. Gerhardtæ, K. Ghorbaniæ, W. Giangw,
L. Gladstoneæ, M. Glaglaæ, T. Glüsenkampbg, A. Goldschmidtb, G. Golupm,
J. G. Gonzalezan, D. Grantw, Z. Griffithæ, C. Haackæ, A. Haj Ismailz, A. Hallgrenæ,
F. Halzenæ, E. Hansenî, B. Hansmannæ, T. Hansmannæ, K. Hansonæ, J. Haugenæ,
D. Hebeckerî, D. Heeremanî, K. Helbingbf, R. Hellauerq, S. Hickfordbf, J. Hignightv,
G. C. Hillb, K. D. Hoffmannq, R. Hoffmannbf, K. Holzapfelak, K. Hoshinaæ, V. Huangbc,
M. Huberak, K. Hultqvistæ, S. Inæ, A. Ishiharaö, E. Jacobiæ, G. S. Japardz,
M. Jeongæ, K. Jeroæ, B. J. P. Jonesæ, M. Jurkovicæ, O. Kalekinx, A. Kappesam,
G. Karagiorgiap, T. Kargbg, A. Karleæ, T. Katoriac, U. Katzx, M. Kaueræ, A. Keivaniæ,
J. L. Kelleyæ, J. Kempø, A. Kheirandishæ, M. Kimax, T. Kintscherbg, J. Kirylukaw,
T. Kittlerx, S. R. Kleinæ, G. Kohnenai, R. Koiralaan, H. Kolanoskiî, R. Konietzan,
L. Köpkea, G. Kopperw, S. Kopperbf, D. J. Koskinenl, M. Kowalskiæ, C. B. Kraussw,
K. Kringsak, M. Krollå, G. Krücklauf, C. Krügeræ, J. Kunnenm, S. Kunwarbg,
N. Kurahashia, T. Kuwabaraö, M. Labarez, J. L. Lanfranchibc, M. J. Larsont,
F. Lauberbf, D. Lennartzv, M. Lesiak-Bzdakaw, M. Leuermannæ, J. Leuneræ, J. LoSeccoæ,
L. Luo, J. Lünenmannm, J. Madsenau, G. Maggiqm, K. B. M. Mahnv, S. Mancinaæ,
S. Mandaliaæ, B. Mandelartzj, S. Markap, Z. Markasp, R. Maruyamaao, K. Maseö,
R. Maunu, F. McNally, K. Meagher, M. Medici, M. Meier, A. Meli, T. Menne, G. Merino, T. Meures, S. Miarecki, L. Mohrmann, T. Montaruli, R. W. Moore, M. Moulai, R. Nahnhauer, U. Naumann, G. Neer, H. Niederhausen, S. Nowicki, D. R. Nygren, A. Obertacke Pollmann, A. Olivas, A. O’Murchadha, A. Palazzo, T. Palczewski, H. Pandya, D. V. Pankova, Œ. Penek, J. A. Pepper, C. P´erez de los Heros, T. C. Petersen, D. Pieloth, E. Pinat, J. L. Pinfold, P. B. Price, G. T. Przybylski, M. Quinnan, C. Raab, L. R¨adel, M. Rameez, K. Rawlins, R. Reimann, B. Relethford, A. Olivas, A. O’Murchadha, T. Schmidt, S. Schoenen, S. Schoneberg, L. Schumacher, D. Seckel, S. Seunarine, M. H. Shaevitz, D. Soldin, S. Söldner-Rembold, M. Song, G. M. Spiczak, C. Spiering, M. Stahlberg, T. Stanev, A. Stasik, A. Steuer, T. Stezelberger, R. G. Stokstad, A. Stößl, R. Ström, N. L. Strojohann, G. W. Sullivan, M. Sutherland, H. Taavola, I. Taboada, A. Taketa, H. K. M. Tanaka, J. Tata, F. Tenholt, S. Ter-Antonyan, A. Terliuk, G. Tesi, S. Tilav, P. A. Toale, M. N. Tobin, S. Toscano, D. Tosi, M. Tselengidou, A. Turcati, E. Unger, M. Usner, J. Vandenbroucke, N. van Eijndhoven, S. Vanheule, M. van Rossum, J. van Santen, J. Veenkamp, M. Vehring, M. Voge, M. Vraeghe, C. Walck, A. Wallace, M. Wallraff, N. Wandkowsky, Ch. Weaver, M. J. Weiss, C. Wendt, S. Westerhoff, B. J. Whelan, S. Wickmann, K. Wiebe, C. H. Wiebusch, L. Wille, D. R. Williams, L. Wills, M. Wolf, T. R. Wood, E. Woolsey, K. Woschnagg, S. Wren, D. L. Xu, X. W. Xu, Y. Xu, J. P. Yanez, G. Yodh, S. Yoshida, M. Zoll

aIII. Physikalisches Institut, RWTH Aachen University, D-52056 Aachen, Germany
bDepartment of Physics, University of Adelaide, Adelaide, 5005, Australia
cDept. of Physics and Astronomy, University of Alaska Anchorage, 3211 Providence Dr., Anchorage, AK 99508, USA
dCTSPS, Clark-Atlanta University, Atlanta, GA 30314, USA
eSchool of Physics and Center for Relativistic Astrophysics, Georgia Institute of Technology, Atlanta, GA 30332, USA
fDept. of Physics, Southern University, Baton Rouge, LA 70813, USA
ab Dept. of Physics and Astronomy, University of Kansas, Lawrence, KS 66045, USA
ac School of Physics and Astronomy, Queen Mary University of London, London E1 4NS, United Kingdom
ad Dept. of Astronomy, University of Wisconsin, Madison, WI 53706, USA
ae Dept. of Physics and Wisconsin IceCube Particle Astrophysics Center, University of Wisconsin, Madison, WI 53706, USA
af Institute of Physics, University of Mainz, Staudinger Weg 7, D-55099 Mainz, Germany
ag School of Physics and Astronomy, The University of Manchester, Oxford Road, Manchester, M13 9PL, United Kingdom
ah Department of Physics, Marquette University, Milwaukee, WI, 53201, USA
ai Université de Mons, 7000 Mons, Belgium
aj National Research Nuclear University MEPhI (Moscow Engineering Physics Institute), Moscow, Russia
ak Physik-Department, Technische Universität München, D-85748 Garching, Germany
al Max-Planck-Institut für Physik (Werner Heisenberg Institut), Föhringer Ring 6, D-80805 München, Germany
am Institut für Kernphysik, Westfälische Wilhelms-Universität Münster, D-48149 Münster, Germany
an Bartol Research Institute and Dept. of Physics and Astronomy, University of Delaware, Newark, DE 19716, USA
ao Dept. of Physics, Yale University, New Haven, CT 06520, USA
ap Columbia Astrophysics and Nevis Laboratories, Columbia University, New York, NY 10027, USA
aq Dept. of Physics, University of Notre Dame du Lac, 225 Nieuwland Science Hall, Notre Dame, IN 46556-5670, USA
ar Dept. of Physics, University of Oxford, 1 Keble Road, Oxford OX1 3NP, UK
as Dept. of Physics, Drexel University, 3141 Chestnut Street, Philadelphia, PA 19104, USA
at Physics Department, South Dakota School of Mines and Technology, Rapid City, SD 57701, USA
Abstract

The Precision IceCube Next Generation Upgrade (PINGU) is a proposed low-energy infill extension to the IceCube Neutrino Observatory. With detection technology modeled closely on the successful IceCube example, PINGU will provide a 6 Mton effective mass for neutrino detection with an energy threshold of a few GeV. With an unprecedented sample of over 60,000 atmospheric neutrinos per year in this energy range, PINGU will make highly competitive measurements of neutrino oscillation parameters in an energy range over an order of magnitude higher than long-baseline neutrino beam experiments. PINGU will measure the mixing parameters $\theta_{23}$ and $\Delta m^2_{32}$, including the octant of $\theta_{23}$ for a wide range of values, and determine the neutrino mass ordering at 3$\sigma$ median significance within 5 years of operation. PINGU’s high precision measurement of the rate
of $\nu_\tau$ appearance will provide essential tests of the unitarity of the $3 \times 3$ PMNS neutrino mixing matrix. PINGU will also improve the sensitivity of searches for low mass dark matter in the Sun, use neutrino tomography to directly probe the composition of the Earth’s core, and improve IceCube’s sensitivity to neutrinos from Galactic supernovae. Reoptimization of the PINGU design has permitted substantial reduction in both cost and logistical requirements while delivering performance nearly identical to configurations previously studied.

Introduction

Following the discovery of neutrino oscillations which show that neutrinos have mass [1, 2], experiments using neutrinos produced in the atmosphere, in the sun, at accelerators, and at reactors have measured the mixing angles and mass-squared differences that characterize the oscillations between the three known flavors of neutrinos. Several important questions remain: whether the mixing angle $\theta_{23}$ is maximal and, if not, whether $\theta_{23} < 45^\circ$ or $\theta_{23} > 45^\circ$ (the “octant” of $\theta_{23}$), whether the ordering of the mass eigenstates is “normal” or “inverted”, and whether Charge-Parity (CP) symmetry is violated with nonzero $\delta_{\text{CP}}$ in the lepton sector. More fundamentally, a better understanding of neutrino oscillations may shed light on the origins of neutrino mass, the possible relationship of neutrinos to the matter-antimatter asymmetry of the universe, and probe new physics beyond the Standard Model.

The Precision IceCube Next Generation Upgrade (PINGU) will provide unprecedented sensitivity to a broad range of neutrino oscillation parameters. Embedded in the existing IceCube/DeepCore subarray, with an energy threshold of less than 5 GeV, PINGU will make highly competitive measurements of atmospheric mixing parameters, the octant of $\theta_{23}$, $\nu_\tau$ appearance, and the neutrino mass ordering (NMO, also referred to as the neutrino mass hierarchy), through studies of a range of neutrino energies and path lengths which cannot be probed by long-baseline or reactor neutrino experiments. PINGU will also improve the sensitivity of IceCube to neutrino bursts from supernovae and to neutrinos produced by dark matter annihilations.

In the past few years, in addition to the discovery of high energy neutrinos of astrophysical origin [3], the IceCube Collaboration has made competitive measurements of neutrino oscillations [4, 5] and searches for dark matter [6]. The technologies for drilling holes, deploying instruments, and detecting neutrinos in the deep Antarctic ice are proven, and
the costs and risks of constructing PINGU are moderate and well understood. As an extension of the IceCube detector, the incremental operational costs of PINGU would be correspondingly low.

The South Pole Station and the IceCube Neutrino Observatory

Over the past decade, the South Pole has emerged as a world-class site for astronomy, particle astrophysics and neutrino oscillation physics. At the Amundsen-Scott South Pole Station the glacial ice is more than 2.8 km thick, radiopure, and optically clear [7], enabling the construction of a neutrino telescope of unprecedented scale. The IceCube Neutrino Observatory, the world’s largest neutrino detector, has been in full operation since 2011. IceCube uses 5160 optical sensors attached to 86 vertical “strings” (cables) to transform one billion tons of Antarctic ice into a Cherenkov radiation detector. The sensor modules were deployed using a hot water drill to melt holes 2.5 km deep in the ice, with the modules deployed at depths of 1.5–2.5 km below the surface. The NSF’s Amundsen-Scott Station provides comprehensive infrastructure for IceCube’s scientific activities, including the IceCube Laboratory building that houses power, communications, and data acquisition systems, shown in Fig. 1.

The Antarctic ice cap permits very large volumes of material to be instrumented at relatively low cost. DeepCore, the low energy subarray of IceCube, is located at the bottom center of the array and observes some 20,000 neutrinos per year at energies below 50 GeV,
incident from all directions. The temperature and radiopurity of the ice greatly reduce thermionic and radioactive noise in the photomultiplier tubes (PMTs), the fundamental building block of the IceCube detector, aiding in the observation of lower energy neutrinos. The outermost IceCube sensors detect and enable an active veto of incoming atmospheric muons, reducing muon background rates in the deep detector to levels comparable to those in deep mines.

PINGU Design

PINGU will greatly enhance IceCube’s capabilities below a neutrino energy of 50 GeV with the deployment of additional photodetector modules within DeepCore, over an instrumented volume of 6 Mton. With an energy threshold of a few GeV, PINGU will substantially improve precision for neutrino events below 20 GeV — the key energy range for measurements of the atmospheric neutrino oscillation patterns and detection of the imprint of the neutrino mass ordering on these patterns. PINGU has a number of attractive features:

- No state-of-the-art development required
- > 10 years experience of IceCube installation and operations
- Performance and cost estimates based on existing detector and tools
- Low marginal cost of operations, leveraging IceCube infrastructure
- Near 100% duty factor
- > 60,000 neutrino events/year
- > 3,000 $\nu_\tau$ events per year
- Broad sensitivity to new physics through observation of a wide range of neutrino energies and baselines

PINGU leverages the experience gained from designing, deploying and operating IceCube, enabling a rapid construction time with minimal risk and at relatively modest expense. The recent development of the capability to deliver cargo and fuel to the station via overland traverse rather than aircraft, as well as planned improvements in drilling efficiency
and sensor power requirements, make the logistical and operational footprint of PINGU significantly smaller than that of IceCube both during and after construction.

Initial studies of PINGU performance [8] showed that PINGU would deliver a world-class 6 Mton water Cherenkov detector for a cost below US$100M. Those projections were based on a configuration of 40 new strings, each mounting 96 optical modules. Our recent studies have shown that a geometry that concentrates a slightly larger amount of PMT photocathode area on fewer strings provides the same sensitivity while reducing both costs and logistical support requirements significantly. A schematic of this design is shown in Fig. 2. Based on our experience with IceCube, in which 18–20 strings were deployed per season once construction was underway, 26 strings of 192 optical modules each could be installed at the South Pole in two deployment seasons. This configuration would provide nearly identical performance to the original 40-string design. Even a reduced 20 string geometry, which could be deployed in two seasons with considerable schedule contingency, would still enable the essential scientific program, even though it would provide less precise event reconstruction and reduced performance compared to the projections presented here.

The studies presented in this document are based on the new, less expensive 26-string configuration. In this configuration, PINGU will be composed of sensors similar in shape and size to those already deployed in IceCube, enabling deployment with nearly identical techniques and equipment. For the purposes of this study, a sensor identical to the current IceCube DOM [9, 10] has been assumed. This would require only modest updates to the electronics to be used in PINGU. We are also evaluating the possibility of replacing the optical modules with multi-PMT mDOMs [11, 12]. A string consisting of 125 mDOMs would provide 40% more photocathode area, as well as directional information on the arriving photons, for the same cost as a string of 192 regular optical modules. This promises further potential improvements over current performance projections.

The existing IceCube DOMs that will surround PINGU will provide a highly effective active veto against downward-going cosmic ray muons, the chief background for all PINGU physics channels, a strategy successfully developed for DeepCore measurements [5]. The surrounding instrumentation will also provide containment of muons up to $E_\mu \sim 100$ GeV, improving energy resolution and utilizing the existing IceCube detector to substantially improve PINGU’s performance relative to a stand-alone instrument. PINGU will be designed as an extension of IceCube, closely integrated with IceCube’s online and offline systems, leading to a very low incremental cost of operation.
Figure 2: Schematic layout of PINGU within the IceCube DeepCore detector. In the top view inset at right, black circles mark standard IceCube strings, on a 125 m hexagonal grid. Blue squares indicate existing DeepCore strings, and red crosses show proposed PINGU string locations. PINGU modules would be deployed in the clearest ice at the bottom of the detector, as shown in the vertical profile at bottom, with vertical spacing several times denser than DeepCore.
PINGU will provide an effective detector target mass of 6 Mton for $\nu_\mu$ charged-current interactions, fully efficient above 8 GeV and 50% efficient at $\sim$3 GeV, yielding data samples of approximately 65,000 upgoing neutrinos per year at energies below 80 GeV. On average, a 10 GeV $\nu_\mu$ CC event will produce 90 Cherenkov photons detected by PINGU; existing IceCube reconstruction algorithms applied to simulated PINGU events yield an energy resolution $\Delta E/E$ of 20% and an angular resolution of around 15° for such events.

PINGU Science

The primary scientific goal of PINGU is the observation of neutrino oscillations using the atmospheric neutrino flux. Several key parameters will be measured by PINGU, including the mixing angles and mass-squared splittings associated with both muon neutrino disappearance and tau neutrino appearance, the octant of the mixing angle $\theta_{23}$, and the ordering of the neutrino mass eigenstates.

With neutrino path lengths through the Earth ranging up to 12,700 km, PINGU will observe the same oscillation phenomena at energies and baselines an order of magnitude larger than current and planned long-baseline neutrino beam experiments, as illustrated in Fig. 3. PINGU thus complements accelerator and reactor neutrino experiments, as the different set of systematic uncertainties confronting PINGU and the weak impact of $\delta_{\text{CP}}$ on PINGU measurements will lend robustness to global determination of neutrino oscillation parameters. Comparison of PINGU observations to those made by both currently running experiments such as T2K and NO$\nu$A and planned experiments such as DUNE, Hyper-Kamiokande, JUNO and KM3NeT / ORCA [13] will also provide broad and model-independent potential for discovery of new physics. Finally, PINGU will have unprecedented sensitivity to tau neutrino appearance. Compared to the 180 charged current tau neutrino interactions observed in 2,806 days of Super-Kamiokande data [14], PINGU will be able to detect almost 3,000 such interactions every year.

The performance projections presented here are a summary of detailed studies described in a more comprehensive document [15], which will be available shortly. They are based on full Monte Carlo simulations and detailed reconstructions, including the full detector model developed over 10 years of experience operating the IceCube detector. The full suite of systematic uncertainties used for IceCube data analysis have been taken into account in these studies.
Figure 3: Energy ranges and baselines of operational and planned neutrino oscillation experiments. The diagonal lines indicate the characteristic oscillation scales $L_\odot$ set by the solar mass-squared splitting $\Delta m_{21}^2$ (dashed) and $L_{\text{atm}}$ set by the atmospheric mass-squared splitting $\Delta m_{32}^2$ (dot-dashed). The 3.5 GeV threshold for $\tau$ lepton production in $\nu_\tau$ CC events is shown by a vertical line. The energy ranges covered by the KM3NeT ORCA and ARCA detectors are indicated by bars above the plot for clarity. For Super-Kamiokande, ORCA, and PINGU, the upper end of the energy range is that at which the $\nu_\mu$ energy resolution degrades because muons are no longer contained within the detector. For IceCube and PINGU, this energy is marked by the vertical dashed line.
Atmospheric Oscillation Measurements

The “atmospheric” mixing between the second and third neutrino mass eigenstates, which produced the first strong evidence that neutrinos oscillate between flavors, is now the least well measured channel of neutrino oscillation. Current measurements of the atmospheric mixing parameters $\sin^2(\theta_{23})$ and $\Delta m_{32}^2$ by IceCube [5], MINOS [16], T2K [17], NO$\nu$A [18], and Super-Kamiokande [19] are shown in Fig. 4.

PINGU will measure the atmospheric parameters primarily through the disappearance of $\nu_\mu$ from the atmospheric flux at energies above 5 GeV; Fig. 5 shows the disappearance that will be observed by PINGU in the cascade and track samples as a function of $L_{\text{reco}}/E_{\text{reco}}$, the reconstructed ratio of the neutrino travel distance to its energy. With increased photocathode density providing a lower energy threshold and significantly improved event reconstruction compared to current IceCube measurements [5], PINGU will determine these parameters with precision comparable to or better than that expected from current accelerator-based experiments (Fig. 6), but at much higher energies and over a range of very long baselines. This will provide world-class sensitivity to these parame-
Figure 5: The disappearance, caused by standard neutrino oscillations, that will be observed by PINGU in the cascade (top) and track (bottom) samples, as a function of the ratio of the reconstructed neutrino travel distance to its reconstructed energy. The gray bands show the sizes of the statistical uncertainties.

Maximal Mixing and the $\theta_{23}$ Octant

Current measurements of the mixing angle $\theta_{23}$, which specifies the relative amounts of the $\nu_\mu$ and $\nu_\tau$ flavors in the third neutrino mass eigenstate, suggest that the angle is close to 45° (corresponding to equal contributions from the two flavors). This possibility is known as “maximal mixing” and could reflect a new fundamental symmetry. If $\theta_{23}$ is not exactly
Figure 6: The atmospheric neutrino oscillation contours are shown under assumptions of both the (a) normal and (b) inverted orderings. Both orderings show the effect of different assumed true values: the Fogli 2012 [22] and NuFit 2014 [23] global fits, and maximal mixing. The normal ordering assumption includes projected sensitivities from NO\(\nu\)A (95% CL, first octant only) [24] and T2K [25] assuming \(\delta_{CP} = 0\). For NO\(\nu\)A, the second octant would be ruled out at 90% CL under this assumption.

45°, determining its value and whether it is slightly more or less than 45° (its “octant”) is of great interest for understanding the origin of neutrino masses and mixing [26]. In the simple two-flavor oscillation model, values of \(\theta_{23}\) above and below 45° produce identical transition probabilities. However, this degeneracy is broken for three-flavor oscillations in the presence of matter due to the large value of \(\theta_{13}\).

Neutrino beam experiments such as NO\(\nu\)A and T2K can probe the \(\theta_{23}\) octant by comparison of \(\nu_e\) appearance rates for neutrinos and antineutrinos. However, as the matter effects at the energies and baselines of those experiments are relatively weak, the sensitivity to the octant depends considerably on the CP-violating parameter \(\delta_{CP}\). By contrast, PINGU will determine the octant by comparison of \(\nu_\mu \rightarrow \nu_\mu\) and \(\nu_\mu \rightarrow \nu_e\) transition probabilities for neutrinos and antineutrinos passing through the Earth’s core and mantle [27, 28, 29, 30, 31]. The resonant matter effect on the conversion rates breaks the octant degeneracy, and the value of \(\delta_{CP}\) has little impact on PINGU observations.

The sensitivity of PINGU to the \(\theta_{23}\) octant is shown in Fig. 7. If the neutrino mass ordering, discussed in detail below, is normal, PINGU’s sensitivity is slightly better than expected for the combined T2K and NO\(\nu\)A data sets [32]. If the mass ordering is inverted, PINGU is somewhat less sensitive than the long-baseline experiments as the matter res-
Figure 7: Amount of PINGU data required to determine the $\theta_{23}$ octant (i.e., to exclude the wrong octant at 90% C.L.), as a function of the true mass ordering and true value of $\sin^2(\theta_{23})$. Sensitivity is lower if the ordering is inverted as the matter resonance affects antineutrinos rather than neutrinos. The value of $\delta_{CP}$ has minimal impact and is assumed to be zero.

...onance affects antineutrinos. In either case, PINGU can determine the octant for a wide range of $\theta_{23}$, and for values close to maximal mixing PINGU data will be highly complementary to the long baseline information due to the different sources of degeneracy — $\delta_{CP}$ for the beam experiments vs. the mass ordering for PINGU.

**The Neutrino Mass Ordering**

The ordering of two of the three neutrino mass eigenstates, $m(\nu_2) > m(\nu_1)$, is known from solar neutrino measurements [33], but we do not yet know whether $\nu_3$ is heavier or lighter than the other two eigenstates. This is known as the neutrino mass ordering (NMO) question. The case in which $\nu_3$ is heavier is called the “normal” ordering (NO); if $\nu_3$ is lighter, the ordering is “inverted” (IO).

In addition to its intrinsic interest, the ordering has deep implications for the theoretical understanding of fundamental interactions. Its measurement would assist in discriminating between certain theoretical models at the GUT mass scale [34]. Experimentally, knowledge of the ordering would positively impact ongoing and future research of other crucial neutrino properties: the unknown NMO is a major ambiguity for running or approved accelerator neutrino oscillation experiments with sensitivity to leptonic CP violation [35, 36, 37, 38]. PINGU data are not highly sensitive to $\delta_{CP}$; if included as a
(a) Normal neutrino mass ordering assumed. (b) Inverted neutrino mass ordering assumed.

Figure 8: Expected significance with which the neutrino mass ordering will be determined using four years of data, as a function of the true value of $\sin^2(\theta_{23})$. Solid red (NO) and blue (IO) lines show median significances, while the green and yellow bands indicate the range of significances obtained in 68% and 95% of hypothetical experiments. The significance for determining the ordering when the true ordering is inverted is relatively insensitive to $\theta_{23}$, while for the normal ordering large values of $\theta_{23}$ are advantageous. The range shown corresponds approximately to the current $3\sigma$ allowed region of $\theta_{23}$; the global best-fit values from the NuFit group [23] for both orderings are indicated by black arrows.

completely free nuisance parameter in the analysis, $\delta_{CP}$ reduces the significance of the ordering determination by 10%–20% at most, depending on the true values of $\delta_{CP}$ and $\theta_{23}$. In addition, atmospheric neutrino data from PINGU or other proposed experiments such as INO [39] or ORCA [40] in combination with existing neutrino beam experiments and proposed reactor experiments like JUNO [41] and RENO-50 [42] provide synergistic inputs that can improve the combined significance of the NMO determination beyond the purely statistical addition of results [43, 44, 45]. PINGU’s determination of the NMO is thus highly complementary to other experimental efforts, resolving possible degeneracies between the mass ordering and CP violation and possibly increasing the precision with which CP violation can be measured by long-baseline experiments. In addition, the determination of the NMO will influence the planning and interpretation of non-oscillation experiments (neutrinoless double $\beta$ decay and $\beta$ decay) sensitive to the particle nature of the neutrino (Dirac vs Majorana) and/or its absolute mass [46], and help to test popular see-saw neutrino mass models and the related mechanism of leptogenesis in the early universe [47].

With a neutrino energy threshold below 5 GeV, PINGU will be able to determine the NMO using the altered flavor composition of atmospheric neutrinos that undergo Mikheyev-Smirnov-Wolfenstein (MSW) [48, 49] and parametric [50] oscillations as they pass through the Earth. At energies of approximately 5–20 GeV, the alteration of the oscillation pat-
terns of both $\nu_\mu$ and $\nu_e$ events is strong enough to enable PINGU to determine whether the neutrino mass ordering is normal or inverted. Given the current global best fit values of the oscillation parameters, PINGU will determine the ordering with a median significance of $3\sigma$ in approximately 5 years. The significance derived from any actual measurement is subject to large statistical fluctuations, illustrated for PINGU in Fig. 8, so that multiple experimental efforts to measure the ordering are required to guarantee it is determined quickly. For PINGU, the expected significance also depends strongly on the actual value of $\theta_{23}$, which is not well known. The expectation of 5 years to reach $3\sigma$ significance is conservative in the sense that PINGU’s sensitivity to the NMO would be greater in almost any region of the allowed parameter space of $\theta_{23}$ other than the current global best fit, as shown in Fig. 8.

Unitarity of the Neutrino Mixing Matrix

In the standard neutrino oscillation picture, atmospheric $\nu_\mu$ disappearance arises primarily from $\nu_\mu \rightarrow \nu_\tau$ oscillations. However, in contrast to the CKM matrix in the quark sector, the unitarity of the mixing between the three known neutrino flavors has not been experimentally verified. Many theories of physics beyond the Standard Model include massive fermionic singlets which could mix with neutrinos, expanding the standard $3 \times 3$ PMNS neutrino mixing matrix into an extended $(3 + N) \times (3 + N)$ matrix and implying that the $3 \times 3$ PMNS submatrix is non-unitary. The unitarity of PMNS mixing has only been tested at the 20%-40% level, primarily due to the lack of direct measurements of $\nu_\tau$ oscillations [51]. An extended mixing matrix could either decrease or moderately increase the rate of $\nu_\tau$ appearance relative to the Standard Model expectation. Notably, both the current measurements of $\nu_\tau$ appearance somewhat exceed the expected appearance rate, as shown in Fig. 9.

The relatively high mass of the $\tau$ lepton greatly reduces the interaction rate of $\nu_\tau$ at low energies: current measurements of $\nu_\tau$ appearance rates are based on data sets including 180 and 5 $\nu_\tau$ events in Super-K [14] and OPERAs [52], respectively. Tau neutrino appearance on baselines comparable to the Earth’s diameter gives rise to large numbers of $\nu_\tau$ with energies around 20 GeV, well above PINGU’s energy threshold. PINGU is expected to detect nearly 3,000 $\nu_\tau$ CC interactions per year. These $\nu_\tau$ events can be distinguished from the background of $\nu_e$ and $\nu_\mu$ CC and NC events by their characteristic angular distribution and energy spectrum, arising from their appearance via flavor oscillation at specific $L_\nu/E_\nu$ (the ratio of the neutrino’s path length through the Earth to its energy). This allows PINGU to measure the rate of $\nu_\tau$ appearance with a precision of better than
Figure 9: Precision with which the rate of $\nu_\tau$ appearance can be measured, in terms of the PMNS expected rate, as a function of exposure (in months). The true value is assumed to be 1.0 (the standard expectation) for illustration. The expected $\pm 1\sigma$ and $\pm 2\sigma$ regions and $\pm 5\sigma$ limits are shown, as well as current measurements by Super-K [14] and OPERA [52].

10% with one year of data, as shown in Fig. 9, providing a significantly more precise probe of PMNS matrix elements in the $\nu_\mu$ and $\nu_\tau$ rows than previous experiments. The measurement could either strengthen the 3-flavor model and the underlying unitarity of its corresponding mixing, or point us in the direction of new physics due to sterile neutrinos, non-standard interactions, or other effects.

Additional PINGU Science: Dark Matter, Tomography and Supernovae

By virtue of its GeV-scale neutrino energy threshold, PINGU will have sensitivity to annihilations of dark matter accreted by the Sun with mass as low as 5 GeV. In this neutrino energy regime, PINGU will also establish a new experimental technique for direct tomographic measurement of the Earth’s composition through the faint imprint of the core’s proton-neutron ratio on neutrino oscillations [53, 54]. Neutrino oscillation tomography relies on the MSW effect, which depends on the electron density. Seismic measurements by contrast are sensitive to the mass density and have resulted in a very precise determination of the Earth matter density profile, so the composition can be extracted from comparison of the two measurements. Although this technique is affected by unknown neutrino physics, especially the octant of $\theta_{23}$, information regarding the
Earth’s composition can be extracted with uncertainties in the oscillation physics and density profile treated as nuisance parameters. As global understanding of the neutrino physics improves, more precise composition measurements will be possible.

The increased density of instrumentation in PINGU compared to IceCube and DeepCore will also enhance the observatory’s sensitivity to bursts of low energy (∼ 15 MeV) supernova neutrinos. These neutrinos are not detected individually, but rather observed as a detector-wide increase in count rates due to the collective effect of light deposited in the detector as the neutrino burst arrives [55]. Some information about the neutrino energy spectrum can be obtained by comparing the rate at which immediately neighboring DOMs detect light in close temporal coincidence, indicative of a brighter neutrino event, to the overall count rate [56, 57]. The PINGU instrumentation will provide an improvement in the sensitivity for detecting supernovae of a factor of two and, due to the closer DOM spacing, a factor of five in the precision of the measured average neutrino energy [15].

Cost, Schedule, and Logistics

The 26 string configuration of PINGU substantially reduces costs in several areas compared to the original 40 string configuration. First, personnel costs associated with deployment are reduced significantly by the elimination of the third drilling season. Second, although the number of optical modules increases slightly, other costs (cables, fuel for the hot water drill, and logistical support) scale with the number of holes and are cut by almost half. Finally, the reduced scope will allow us to refurbish the existing IceCube hot water drill for reuse, rather than building a full replacement.

Many components of the hot water drill used to install IceCube remain available at the South Pole Station or in McMurdo Station, and reusing them will greatly reduce the total project cost. The formation of bubbles in the re-frozen ice surrounding the optical modules is a leading source of systematic uncertainty in IceCube data analyses. The drill will be refurbished and a modified drill melting profile will be used that will significantly reduce the quantity of dissolved gases introduced into the detector region. A water filtration and degassing stage will be added to the drill to assist in removing any remaining residual gases, thus limiting bubble formation. The total cost of drill refurbishment and deployment operations is approximately US$10M. The instrumentation for each string costs approximately US$1.2M; it is anticipated that the bulk of the instrumentation would be provided by non-US participants. Project management and other associated costs are expected to come to an additional US$5M. A summary of costs is shown in Table 1.
Table 1: Summary costs in USD, excluding fuel and contingency, for construction of PINGU. It is expected that non-US partners will provide the bulk of the instrumentation whose total cost is shown in the table. Drill refurbishment and deployment include the labor of the scientists and engineers associated with the hot water drill and string installation effort. Instrumentation costs include labor for module assembly, which contributes slightly over $1M to the total. Fuel requirements for the hot water drill are provided as volumes due to uncertainties in the price of oil and the impact of the overland traverse on transport costs; recent costs are approximately $20/gal.

We anticipate that two years will be required for refurbishment and improvement of the hot water drill. Optical module assembly and transportation to the South Pole would occur in parallel. Once the drill and optical modules are available at the South Pole, the full PINGU array can be deployed in two seasons of activity. Some preparatory activity (snow compacting, firn drilling) would be required in the preceding South Pole season to enable a prompt start to deployment once the drill arrives. A summary of the schedule is shown in Figure 10.

In contrast to the construction of the IceCube Observatory, for which all cargo and fuel had to be airlifted to the South Pole Station, nearly all materials required for PINGU construction would be transported to the Pole via overland traverse. In addition, improvements in electronics design permit a substantial reduction in power consumption by PINGU optical modules compared to IceCube DOMs. Both of these advances will greatly reduce the impact on Antarctic Program logistics, as well as reducing costs.

Conclusion

PINGU will be a world-class instrument for neutrino oscillation physics exploring an energy and baseline range that cannot be probed by long-baseline neutrino beam experiments. PINGU will make a leading measurement of the atmospheric neutrino oscillation parameters, test the maximal mixing hypothesis, provide significantly improved
constraints on the unitarity of the Standard Model neutrino mixing matrix, and determine the mass ordering with an expected significance of $3\sigma$ within 5 years. PINGU observations of high energy atmospheric neutrinos will be highly complementary to existing and planned long-baseline and reactor neutrino experiments, providing a robust validation with very different systematic uncertainties as well as sensitivity to potential new physics. PINGU will also extend IceCube’s reach in searches for dark matter annihilation to low mass particles, increase our sensitivity to neutrino bursts from supernovae, and provide a first-ever tomographic probe of the Earth’s core.

Building on prior experience with IceCube and DeepCore, the risks associated with instrumentation design, drilling, and deployment are well understood and proven to be manageable. Likewise, the estimated cost is well grounded in knowledge gained in the design and construction of IceCube. The performance projections shown here are based on full detector simulation and reconstruction algorithms informed by a decade of experience operating IceCube. Moreover, there is potential for further improvements in the future using a detector based on multi-PMT DOMs.

Acknowledgements

We acknowledge the support from the following agencies: U.S. National Science Foundation-Office of Polar Programs, U.S. National Science Foundation-Physics Division, University
of Wisconsin Alumni Research Foundation, the Grid Laboratory of Wisconsin (GLOW) grid infrastructure at the University of Wisconsin - Madison, the Open Science Grid (OSG) grid infrastructure; U.S. Department of Energy, and National Energy Research Scientific Computing Center, the Louisiana Optical Network Initiative (LONI) grid computing resources; Natural Sciences and Engineering Research Council of Canada, WestGrid and Compute/Calcul Canada; Swedish Research Council, Swedish Polar Research Secretariat, Swedish National Infrastructure for Computing (SNIC), and Knut and Alice Wallenberg Foundation, Sweden; German Ministry for Education and Research (BMBF), Deutsche Forschungsgemeinschaft (DFG), Helmholtz Alliance for Astroparticle Physics (HAP), Research Department of Plasmas with Complex Interactions (Bochum), Germany; Fund for Scientific Research (FNRS-FWO), FWO Odysseus programme, Flanders Institute to encourage scientific and technological research in industry (IWT), Belgian Federal Science Policy Office (Belspo); Science and Technology Facilities Council (STFC) and University of Oxford, United Kingdom; Marsden Fund, New Zealand; Australian Research Council; Japan Society for Promotion of Science (JSPS); the Swiss National Science Foundation (SNSF), Switzerland; National Research Foundation of Korea (NRF); Villum Fonden, Danish National Research Foundation (DNRF), Denmark.
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