Revealing Hidden Orbital Pseudospin Texture with Time-Reversal Dichroism in Photoelectron Angular Distributions

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We performed angle-resolved photoemission spectroscopy (ARPES) of bulk 2H-WSe2 for different crystal orientations linked to each other by time-reversal symmetry. We introduce a new observable called time-reversal dichroism in photoelectron angular distributions (TRDAD), which quantifies the modulation of the photoemission intensity upon effective time-reversal operation. We demonstrate that the hidden orbital pseudospin texture leaves its imprint on TRDAD, due to multiple orbital interference effects in photoemission. Our experimental results are in quantitative agreement with both the tight-binding model and state-of-the-art fully relativistic calculations performed using the one-step model of photoemission. While spin-resolved ARPES probes the spin component of entangled spin-orbital texture in multiorbital systems, we unambiguously demonstrate that TRDAD reveals its orbital pseudospin texture counterpart.

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Locking between spin and valley degrees of freedom emerges in solids possessing a combined broken inversion symmetry and strong spin-orbit coupling, leading to peculiar valley-dependent spin texture in momentum space. This spin-valley locking leads to optical selection rules allowing for the generation of spin- and valley-polarized excited carriers [1–3], which can be used for all-optical selective spin injection [4,5]. In multiorbital systems, additional locking between crystal momentum and orbital degree of freedom emerges as a consequence of band hybridization, leading to complex entangled spin-orbital textures, as predicted in some topological insulators [6,7], two-dimensional electron gases [8], and transition metal dichalcogenides (TMDCs). The resulting momentum-space orbital texture can lead to the orbital Hall effect [9], the orbital Rashba effect [10], and the emergence of orbital Hall insulating phases [11]. Orbitronics [12], i.e., encoding (quantum) information in the orbital degree of freedom, can be seen as a newly emerging field, in analogy to spin- and valleytronics [13,14].

TMDC monolayers are emblematic materials with entangled spin, orbital, and valley degrees of freedom. In a minimal electronic structure model of TMDC monolayers [15], the valence band at the Brillouin zone boundary (K/K′ points) can be described by |ψk⟩ = (|C0(k)|d12⟩ + |C±2(k)|d22⟩) ⊗ |↑/↓⟩VBI + (|C0(k)|d12⟩ + |C±2(k)|d22⟩) ⊗ |↓/↑⟩VB2, where the label VBI and VB2 represented the two first spin-orbit split valence bands and where |d12⟩ = |i|d1⟩ ± |i|d2⟩)/√2. While the spin texture is determined by the momentum-dependent spin state, the orbital texture is set by the momentum-dependent orbital pseudospin, defined as σK/’K′(k) = ⟨ψK/’K′|σi|ψK/’K⟩, where σi (i = x, y, z) is the Pauli operator [16] and where x and y are in-plane and z- out-of-plane coordinates (normal to the surface).

K and K′ valleys are related to each other via the time-reversal operator, i.e., T|ψK⟩ = |ψK’⟩. In TMDC monolayers, swapping valley indexes (time reversal), thus, reverses both the spin and orbital textures. In bulk TMDC of 2H polytype, the adjacent layers are rotated by 180° with respect to each other, leading to opposite and alternating local spin polarization and orbital texture between neighboring layers. This peculiar layered structure naturally introduces the concept of “hidden” spin and...
orbital texture, which exists within each layer but vanishes in the bulk, i.e., when the inversion symmetry of the crystal is restored [17]. Probing such hidden physical properties is experimentally challenging. While spin- and angle-resolved photoemission spectroscopy is now a well-established surface-sensitive technique to investigate hidden spin texture [18–20], an experimental technique allowing one to selectively and directly probe hidden orbital texture has not been established.

In this Letter, we perform extreme ultraviolet (XUV) angle-resolved photoemission spectroscopy (ARPES) of bulk 2H-WSe2 for crystal orientations rotated by α = 60° with respect to each others (R60°) effectively acting as the time-reversal operator (T): \( T_{\alpha} |\psi_k^i\rangle = \hat{T} |\psi_k^j\rangle = |\psi_k^K\rangle \). We introduce a novel observable, time-reversal dichroism in photoelectron angular distributions (TRDAD), which probes the modulation of the photoemission intensity upon time reversal and which is shown to be sensitive to the orbital pseudospin texture, due to multiple orbital interference effects in photoemission. We show that TRDAD is free of any spurious contribution from experimental geometry, which typically complicates the interpretation of the (linear or circular) dichroism in ARPES. Our experimental results are in quantitative agreement with state-of-the-art fully relativistic Korringa-Kohn-Rostoker (KKR) calculations performed using the one-step model of photoemission [21,22] and with a tight-binding model, which allows us to investigate the microscopic origins of TRDAD. While we introduce this novel observable using the emblematic bulk 2H-WSe2 crystal, our conclusions are fully general and TRDAD can be used to probe (hidden) orbital texture in any multiorbital systems.

The experimental apparatus features a tabletop femtosecond (fs) XUV (21.7 eV, 110 meV FWHM bandwidth) beam line [23] coupled to a time-of-flight momentum microscope spectrometer (METIS 1000, SPECS GmbH); see Fig. 1(a). This detector allows for simultaneous detection of the full first Brillouin zone, over an extended binding energy range, without the need to rearrange the sample geometry [24]. More details about the experimental setup can be found elsewhere [23,25,26] and in Supplemental Material [27]. As shown in Figs. 1(b)–1(e), we recorded the 3D photoemission intensity for two different crystal orientations, rotated by 60° with respect to each other. Looking at the experimentally measured constant energy contours (CECs) for energy \( E - E_{\text{VBM}} = -0.25 \text{ eV} \), one can see that the photoemission intensity is strongly anisotropic around each \( K/K' \) valley, describing “croissant-shaped” patterns. This has been previously explained as originating from interference between photoelectrons emitted from the transition metal d-type orbitals [28]. The azimuthal variation of the photoemission intensity around \( K/K' \) points, i.e., the orientation of the croissant, changes upon rotation of the crystal by 60°. A modification of the momentum-resolved photoemission intensity upon time reversal can also be seen for larger binding energies in Figs. 1(d) and 1(e).

Dichroisms in the angular distribution [both linear (LDAD) and circular (CDAD)] are powerful quantities relying on the modulation of the photoemission transition dipole matrix element upon the change of the ionizing radiation polarization state. CDAD has been used to probe electronic chirality in graphene [29], helical spin texture in a topological insulator [30], and Berry curvature in TMDCs [31,32], for example. LDAD is typically assumed to encode the nonrelativistic symmetry of the ground state wave function [33–35], which can contain information about the orbital texture [36,37]. However, dichroism can also
have an extrinsic origin; i.e., it can also emerge from experimental geometry-induced symmetry breaking. Disentangling the intrinsic and extrinsic contribution to the dichroic signal is very challenging but of fundamental importance to extract meaningful physical insight from it.

Using our multidimensional detection scheme with the p-polarized femtosecond XUV pulses incident in the $k_x - k_z$ plane (and along $\Gamma - M - M'$), the normalized intensity differences between the forward [$I_{\alpha}(k_x, k_y, E_B)$] and backward [$I_{\alpha}(-k_x, k_y, E_B)$] hemispheres, i.e., the linear dichroism asymmetry in the photoelectron angular distribution [$A_{\alpha}^{LDAD}(k_x, k_y, E_B)$], can be extracted [see Eq. (1)], without the need to rearrange the sample geometry or the light-polarization state [38,39]:

$$A_{\alpha}^{LDAD} = \frac{I_{\alpha}(k_x, k_y, E_B) - I_{\alpha}(-k_x, k_y, E_B)}{I_{\alpha}(k_x, k_y, E_B) + I_{\alpha}(-k_x, k_y, E_B)}.$$  \hspace{1cm} (1)

Looking at $A_{\alpha}^{LDAD}$ and $A_{\alpha}^{60^\circ}$ [Figs. 2(d) and 2(e)], one can notice that some features of the dichroism are invariant upon time reversal, while others show antisymmetric behavior (sign flip). This can be understood by the fact that the contribution to the dichroism originating from experimental geometry remains unchanged upon $60^\circ$ rotation of the crystal. Moreover, depending on the energy-momentum region of the electronic structure sampled in each experimental data voxel, the associated ground state wave function might be invariant upon time reversal. For example, the dichroism emerging from the branches pointing along the $\Gamma - M - M'$ high-symmetry direction, which is of multiorbital character ($\langle p_{z} \pm i|p_{y}\rangle$), switches sign upon crystal rotation. On the other hand, the dichroism emerging from the hexagonal-shaped band surrounding the $\Gamma$ point, which is mostly of single orbital character ($\langle p_{z}\rangle$), does not.

The new observable that we introduce, called time-reversal dichroism in the photoelectron angular distributions (TRDAD), allows us to isolate the antisymmetric part of the $A_{\alpha}^{LDAD}$ dichroism upon time reversal, in order to remove any spurious contributions from experimental geometry. TRDAD is defined as

$$\text{TRDAD} = \frac{A_{\alpha}^{LDAD} - A_{\alpha}^{60^\circ}}{2},$$  \hspace{1cm} (2)

where crystal rotation by an angle $\alpha - \alpha'$ ($R_{\alpha - \alpha'}$) is equivalent to time reversal, i.e., $R_{\alpha - \alpha'} = \tilde{T}$. The resulting TRDAD is shown in Fig. 2(f). The branches pointing along $\Gamma - M$ have opposite $A_{\alpha}^{LDAD}$ with respect to adjacent valleys and dominates the signal, while the signature of the hexagonal-shaped band surrounding the $\Gamma$ point has disappeared. Indeed, a nonvanishing TRDAD signal implies that the state-resolved dichroism changes sign upon time-reversal operation, which we interpret as a switch of the orbital texture.

![FIG. 2. Extraction of the time-reversal dichroism in photoelectron angular distributions (TRDAD). (a),(b) $I_{0^\circ}$ and $I_{60^\circ}$, the CECs for $E - E_{\text{VBM}} = -1.60$ eV, measured for two crystal orientations rotated by $60^\circ$ with respect to each other. (c) $\Delta I/I$, the raw normalized difference, i.e., $(I_{0^\circ} - I_{60^\circ})/(I_{0^\circ} + I_{60^\circ})$ between CECs shown in (a) and (b). (d),(e) $A_{\alpha}^{LDAD}$ and $A_{\alpha}^{60^\circ}$, the “left-right asymmetries,” reflect the photoemission intensity asymmetry between the $k_x < 0$ and $k_x > 0$ hemispheres, for two crystal orientations, respectively, and are calculated using Eq. (1). (f) TRDAD [calculated using Eq. (2)] represents the component of $A_{\alpha}^{LDAD}$, which is antisymmetric upon time reversal (i.e., upon $60^\circ$ azimuthal rotation of the crystal).]

To investigate the microscopic origin of TRDAD, we perform state-of-the-art quantitative one-step photoemission calculations based on fully relativistic density functional theory. The one-step model of photoemission is implemented in the fully relativistic KKR method. The calculated photoemission signal is layer resolved and includes all matrix element effects such as experimental

![FIG. 3. Comparison between experimentally measured and theoretically (KKR) calculated TRDAD. In the upper hemisphere of each panel, the raw photoemission intensity, and in the lower hemisphere, TRDAD. (a)–(d) Experimentally measured photoemission intensity and TRDAD. (e)–(i) Calculated photoemission intensity and TRDAD. (a),(e) $E - E_{\text{VBM}} = -0.20$ eV, (b),(f) $E - E_{\text{VBM}} = -0.75$ eV, (c),(g) $E - E_{\text{VBM}} = -1.60$ eV, and (d),(i) $E - E_{\text{VBM}} = -2.07$ eV. The radius of each constant energy contour corresponds to 1.6 Å⁻¹.]

216404-3
including the photocurrent from the first tungsten (W) layer [Fig. 4(c)] is already enough to almost perfectly reproduce all features of the full calculation, which is in good agreement with the predicted W d-type orbitals nature of the valence band at K/K’ points. These calculations unambiguously confirm that TRDAD probes hidden physical quantities, which are modulated upon time reversal.

Next, we want to fully disentangle the signatures of spin and orbital textures in TRDAD. To do so, we have investigated the photoemission intensity and associated TRDAD in both the fully relativistic and nonrelativistic limit [vanishing spin-orbit coupling (SOC)]. Indeed, SOC is at the origin of the hidden spin polarization of the two topmost valence bands at K/K’ and, thus, of the emergence of the peculiar spin texture in 2H TMDCs. In the limit where SOC vanishes (nonrelativistic limit), the two oppositely spin-polarized topmost valence bands at K/K’ are merging together, leading to the annihilation of the spin polarization but to a conservation of the orbital texture. Because the dominant relativistic corrections scale with 1/c², where c is the speed of light, a straightforward theoretical approach to go from the fully relativistic to the nonrelativistic limit, and thus to modify the strength of SOC, is to modulate the speed of light. In Fig. 4(e), one can see that, in the fully relativistic case, the topmost valence bands at K/K’ are spin-orbit split and have similar TRDAD patterns, already suggesting its sensitivity to orbital texture. Strikingly, the nonrelativistic TRDAD from the degenerate band at K/K’ is identical to the dichroism of the associated topmost valence band in the fully relativistic case. This observation is smoking-gun evidence that TRDAD is a powerful probe of the hidden orbital texture, which exists even in the absence of spin-orbit coupling and, thus, of spin texture.

Last, to get a more intuitive and comprehensive picture of the origin of TRDAD, we employ a third-nearest neighbor tight-binding (TB) model [15], which provides an excellent description of the electronic structure of 2H-WSe₂ close to the K/K’ points. As shown in Fig. 5(a), the TB model, for energies close to the valence band maximum, qualitatively reproduces the measured TRDAD. Our TB analysis unambiguously confirms that TRDAD originates from interference between |dₓ²−ᵧ²⟩ and |dₓz⟩ orbitals, which is characterized by the orbital pseudospin texture (see Supplemental Material [27]). Moreover, as shown in Figs. 5(b) and 5(c), TRDAD is directly linked to the projection of the in-plane orbital pseudospin (black arrows) along the direction of the orbital vector field, which can be derived from the photoemission matrix elements (magenta arrows; see Supplemental Material [27] for details). Indeed, when the orbital pseudospin and the magenta arrow are parallel (antiparallel), TRDAD is positive (negative), while it vanishes when they are orthogonal. Our tight-binding analysis thus provides a direct relationship between the experimentally measured TRDAD and the orbital texture.

The striking similarity between experimental and theoretical results (Fig. 3) confirms that the KKR method accurately describes the ground state properties of bulk 2H-WSe₂ in an extended binding energy range and captures well subleties of the photoemission process, including multiorbital interference effects. Now that the ability of the KKR method to quantitatively reproduce the experimentally measured signals is established, we want to strengthen our assertion that TRDAD in XUV photoemission probes hidden physical quantities, i.e., quantities that are non-vanishing in each constituent layer but that are vanishing in its inversion-symmetric counterpart (bulk). To do so, we investigated the atomic-layer-resolved photocurrent and associated TRDAD. In Fig. 4(a), the photoemission intensity and associated TRDAD emerging from all layers (bulk) are presented. The outer (VB1) and inner (VB2) bands around each K/K’ valley show very similar dichroism, i.e., the same positive or negative (red and blue, respectively) TRDAD patterns. While the TRDAD signal coming from the topmost selenium (Se) atomic layer [Fig. 4(b)] is strongly different from the full calculation [Fig. 4(a)],
FIG. 5. Linking TRDAD and orbital pseudospin texture using a tight-binding framework. (a) TRDAD for an energy $E = E_{\text{VBM}} = -0.20$ eV computed using the tight-binding formalism described in Supplemental Material [27]. (b), (c) TRDAD and in-plane orbital pseudospin (black arrows) around the $K$ and $K'$ valleys, respectively. The magenta dashed arrow represents the orientation of the orbital vector field, which can be derived from the photoemission matrix elements (more details can be found in Supplemental Material [27]). As shown in Eq. (7) of Supplemental Material [27], when the pseudospin texture is parallel (antiparallel) to the orbital vector field, we get a positive (negative) signal, while TRDAD vanishes if they are orthogonal. This relationship provides a direct link between the experimentally measured TRDAD and the in-plane orbital pseudospin.

pseudospin texture, a quantity of paramount importance in the emergence of Berry curvature and topological properties of matter.

In conclusion, we have introduced a novel and fully general robust observable in angle-resolved photoemission spectroscopy called time-reversal dichroism in photoelectron angular distributions, which probes the modulation of the photoemission intensity upon crystal rotation mimicking time reversal. We have demonstrated that the hidden orbital pseudospin texture of prototypical bulk 2H-WSe$_2$ leaves its imprint on TRDAD through the multiorbital interference process in photoemission. This robust observable is free of contributions from experimental geometry and is extremely stable against variation of the photon energy, contrary to most conventional dichroic ARPES signals, e.g., CDAD (see Supplemental Material [27]). Similar to the role of spin-resolved ARPES to experimentally elucidate complex momentum-space spin texture, we envision that TRDAD could emerge as the new standard observable to probe peculiar momentum-space orbital texture in complex multiorbital materials. Moreover, the extension of the approach to time-resolved TRDAD experiments is conceptually straightforward and will give access to the orbital texture of excited states and changes of topological properties of out-of-equilibrium states of matter, on ultrafast timescales [40–44].

All photoemission data used for the presented analysis are publicly available [45].

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The Pauli matrices act on the orbital space of \(|d_{ij}|, |d_{k\ell}\rangle\) at \(K/K'\).

X. Zhang, Q. Liu, J.-W. Luo, A. J. Freeman, and A. Zunger, Nat. Phys. 10, 387 (2014).

J. M. Riley, F. Mazzola, M. Dendzik, M. Michiardi, T. Takayama, L. Bawden, C. Granerød, M. Leandersson, T. Balasubramanian, M. Hoesch, T. K. Kim, H. Takagi, W. Meevasana, P. Hofmann, M. S. Bahramy, J. W. Wells, and P. D. C. King, Nat. Phys. 10, 835 (2014).

E. Razzoli, T. Jaouen, M.-L. Mottas, B. Hildebrand, G. Monney, A. Pison, S. Muff, M. Fanciulli, N. C. Plumb, V. A. Rogalev, V. N. Strocov, J. Mesot, M. Shi, J. H. Dil, H. Beck, and P. Aeby, Phys. Rev. Lett. 118, 086402 (2017).

J. Tu, X. B. Chen, X. Z. Ruan, Y. F. Zhao, H. F. Xu, Z. D. Chen, X. Q. Zhang, X. W. Zhang, J. Wu, L. He, Y. Zhang, R. Zhang, and Y. B. Xu, Phys. Rev. B 101, 035102 (2020).

H. Ebert, D. Ködderitzsch, and J. Minár, Rep. Prog. Phys. 74, 096501 (2011).

J. Braun, J. Minár, and H. Ebert, Phys. Rep. 740, 1 (2018).

M. Puppin, Y. Deng, C. W. Nicholson, J. Feldl, N. B. M. Schröter, H. Vita, P. S. Kirchmann, C. Monney, L. Retting, M. Wolf, and R. Emstörfer, Rev. Sci. Instrum. 90, 023104 (2019).

K. Medjanik, O. Fedchenko, S. Chernov, D. Kutnyakho, M. Ellguth, A. Oelsner, B. Schönhense, T. R. F. Peixoto, P. Lutz, C.-H. Min, F. Reinert, S. Däster, Y. Acremann, J. Viehhaus, W. Wurth, H. J. Elmers, and B. Schönhense, Nat. Mater. 16, 615 (2017).

S. Beaulieu, S. Dong, N. Tancogne-Dejean, M. Dendzik, T. Pincelli, J. Maklar, R. P. Xian, M. A. Sentef, M. Wolf, A. Rubio, L. Retting, and R. Emstörfer, arXiv:2003.04059.

J. Maklar, S. Dong, S. Beaulieu, T. Pincelli, M. Dendzik, Y. W. Windsor, R. P. Xian, M. Wolf, R. Emstörfer, and L. Retting, arXiv:2008.05829.

See Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevLett.125.216404 for details about the ARPES experimental setup, the KKR calculations, and the derivation of the tight-binding model.

H. Rostami, K. Volckaert, N. Lanata, S. K. Mahatha, C. E. Sanders, M. Bianchi, D. Lizzit, L. Bignardi, S. Lizzit, J. A. Miwa, A. V. Balatsky, P. Hofmann, and S. Ulstrup, Phys. Rev. B 100, 235423 (2019).

Y. Liu, G. Bian, T. Miller, and T.-C. Chiang, Phys. Rev. Lett. 107, 166803 (2011).

Y. H. Wang, D. Hsieh, D. Pilon, L. Fu, D. R. Gardner, Y. S. Lee, and N. Gedik, Phys. Rev. Lett. 107, 207602 (2011).

S. Cho, J.-H. Park, J. Hong, J. Jung, B. S. Kim, G. Han, W. Kyung, Y. Kim, S.-K. Mo, J. D. Denlinger, J. H. Shim, J. H. Han, C. Kim, and S. R. Park, Phys. Rev. Lett. 121, 186401 (2018).

M. Schüler, U. De Giovannini, H. Hübener, A. Rubio, M. A. Sentef, and P. Werner, Sci. Adv. 6, eay2730 (2020).

G. Schönhense, Phys. Scr. T 311, 255 (1990).

N. A. Cherepkov and G. Schönhense, Europhys. Lett. 24, 79 (1993).

A. Sterzi, G. Manzoni, A. Crepaldi, F. Cilento, M. Zacchigna, M. Leclerc, P. Bugnon, A. Magrez, H. Berger, L. Petaccia, and F. Parmigiani, J. Electron Spectrosc. Relat. Phenom. 225, 23 (2018).

Y. Cao, J. A. Waugh, X.-W. Zhang, J.-W. Luo, Q. Wang, T. J. Reber, S. K. Mo, Z. Xu, A. Yang, J. Schneeloch, G. D. Gu, M. Brahlek, N. Bansal, S. Oh, A. Zunger, and D. S. Dessau, Nat. Phys. 9, 499 (2013).

C.-H. Min, H. Bentmann, J. N. Neu, P. Eck, S. Moser, T. Figgemeier, M. Unzelmann, K. Kissner, P. Lutz, R. J. Koch, C. Jozwiak, A. Bostwick, E. Rotenberg, R. Thomale, G. Sangiovanni, T. Siegrist, D. Di Sante, and F. Reinert, Phys. Rev. Lett. 122, 116402 (2019).

S. Chernov, K. Medjanik, C. Tusche, D. Kutnyakho, S. Nepijko, A. Oelsner, J. Braun, J. Minár, S. Borek, H. Ebert, H. Elmers, J. Kirschner, and G. Schönhense, Ultrascribopyc 159, 453 (2015).

C. Tusche, P. Goslawski, D. Kutnyakho, M. Ellguth, K. Medjanik, H. J. Elmers, S. Chernov, R. Wallauer, D. Engel, A. Jankowiak, and G. Schönhense, Appl. Phys. Lett. 108, 261602 (2016).

M. A. Sentef, M. Claassen, A. F. Kemper, B. Moritz, T. Oka, J. K. Freericks, and T. P. Devereaux, Nat. Commun. 6, 7047 (2015).

M. Claassen, C. Jia, B. Moritz, and T. P. Devereaux, Nat. Commun. 7, 13074 (2016).

U. De Giovannini, H. Hübener, and A. Rubio, Nano Lett. 16, 7993 (2016).

T. Oka and S. Kitamura, Annu. Rev. Condens. Matter Phys. 10, 387 (2019).

M. Schüler, U. D. Giovannini, H. Hübener, A. Rubio, M. A. Sentef, T. P. Devereaux, and P. Werner, Phys. Rev. X 10, 041013 (2020).

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