Optimum energy harvesting model for bidirectional cognitive radio networks

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Abstract
Wireless devices' energy efficiency and spectrum shortage problem has become a key concern worldwide as the number of wireless devices increases at an unparalleled speed. Wireless energy harvesting technique from traditional radio frequency signals is suitable for extending mobile devices' battery life. This paper investigates a cognitive radio network model where primary users have their specific licensed band, and secondary users equipped with necessary hardware required for energy harvesting can use the licensed band of the primary user by smart sensing capability. Analytical expressions for considered network metrics, namely data rate, outage probability, and energy efficiency, are derived for uplink and downlink scenarios. In addition, optimal transmission power and energy harvesting power are derived for maximum energy efficiency in downlink and uplink scenarios. Numerical results show that outage probability improves high transmission power in the downlink scenario and high harvested power in the uplink scenario. Finally, the result shows that energy efficiency improves using optimum transmission power and energy harvesting power for downlink and uplink scenarios.

Keywords: Cognitive radio network, Data rate, Energy efficiency, Energy harvesting, Outage probability

1 Introduction
The innovation of emerging technologies such as the Internet of Things (IoT), Artificial Intelligence (AI), Cloud computing, and the recent growth of digital communication systems beyond 5G has contributed most to an ever-expanding number of wireless or wired devices [1]. These devices include smart homes, smart appliances, smart agriculture, IoT-based portable health monitoring systems, embedded system for mobile phones [2]. These gadgets require the battery to function smoothly during operation. Consequently, the battery needs to be frequently recharged as the performance duration of the battery is limited. This has become a serious concern as many users, such as healthcare, military, and other crucial users, cannot afford downtime as those users are connected to a thousand other users in real-time. As the number of devices is rapidly increasing, spectrum shortage and energy scarcity have become a significant concern for researchers worldwide [3]. The introduction of cognitive radio (CR) technology, which includes wireless...
energy harvesting (WEH) and smart spectrum sensing, can be a great solution to the existing resource shortage problem [4].

WEH is an emerging new technology where any device equipped with the necessary hardware can harvest energy from various sources such as solar, thermoelectric, radio frequencies (RF), and others [5]. Recently, WEH from RF devices has been powerfully attracted by the focus of researchers worldwide. IoT technology will significantly benefit from WEH; the battery of IoT devices will not be replaced or recharged frequently. Wireless devices can function longer than the expected lifetime using smart WEH techniques, despite being equipped with a traditional battery [6, 7]. On the other hand, CR can intelligently switch between channels or allocate secondary users (SU) to use the licensed frequency bands of primary users (PU) based on smart sensing capability [8]. Typically, SU can detect spectrum holes (idle time slot of PU) using spectrum sensing and efficiently transmit energy and information within the given phase. However, SUs are not allowed to communicate when PU is active in the transmission phase to improve the quality of service of licensed PU and reduce the interference effect. With a WEH-enabled CR network, SU, such as mobile devices, can harvest energy from RF signals generating from the PU transmitter or base station via smart detection. To effectively utilize PU’s signal, both energy harvesting and information can be transferred between PU and SU via simultaneous wireless and information power transfer. Our primary objective is to study the performance analysis of WEH for bidirectional communication in the CR network in this research.

1.1 Related works

WEH is an emerging new technology where any device equipped with the necessary hardware can harvest energy from various sources such as solar, thermoelectric, radio frequencies (RF), and others [5]. Recently, WEH from RF devices has been powerfully attracted by the focus of researchers worldwide. IoT technology will significantly benefit from WEH; the battery of IoT devices will not be replaced or recharged frequently. Wireless devices can function longer than the expected lifetime using smart WEH techniques, despite being equipped with a traditional battery [6, 7]. On the other hand, CR can intelligently switch between channels or allocate secondary users (SU) to use the licensed frequency band; recently, energy harvesting (EH) has emerged as a promising solution provider for traditional wireless communication devices. Newly designed EH circuits can transform RF from conventional sources to usable direct current (DC) power. Researchers are now working on various EH issues of CR networks, such as spectrum sensing, power allocation, and throughput, to find the optimal solution for CR networks.

1.1.1 Time switching technique

Park et al. presented a novel spectrum scheme to increase the overall throughput of CR networks focus on EH circuit on PU and secondary transmitter. Authors have been derived the detection threshold limit for satisfying the energy constraint concerning maximum total throughput [9]. Bhoumick et al. presented mathematical expression of
detection sensing of EH concerning throughput of CR network. Utilization of reused spectrum and comparison between noise powers based on energy detector is also analyzed here [10]. Power allocation strategy and best channel selection scheme for SU is presented in [11], where authors derived the closed-form expression of packet loss probability and packet delay of SU.

Obaid and Fernando developed a new model to provide WEH in CR network, which exploits media access control (MAC) protocol to increase efficiency in CR network [12]. Simulation result indicates that WEH needs to be extracted from high-powered devices such as TV or radio systems instead of low-powered small devices suggested by researchers. The sensing interval problem of free and busy channel in EH-based CR network was formulated in [13] where removed transmitted energy in a time slot acted as a target function. Afterward, the Markov chain model was developed for each sensing interval to find the energy state transition probability. The work in Malek et al. [14] examined the performance of a multiple-input single-output (MISO) network where SU devices are equipped with multiple antennas to harvest energy from the hybrid base station and existing PU network. Besides, the authors derived the closed-form expressions of outage probability of SU network and introduced an optimization problem to reduce the SU outage probability for transmission power. Novel hybrid underlay channel model in secondary SU network with EH capability was studied in Tayel et al. [15]. Besides, closed-form expression for energy transmission and outage probability for the underlay model in Rayleigh fading channel was derived in their works of primary users (PU) based on smart sensing capability [8]. Typically, SU can detect spectrum holes (idle time slot of PU) using spectrum sensing and efficiently transmit energy and information within the given phase. However, SUs are not allowed to communicate when PU is active in the transmission phase to improve the quality of service of licensed PU and reduce the interference effect. With a WEH-enabled CR network, SU, such as mobile devices, can harvest energy from RF signals generating from the PU transmitter or base station via smart detection. To effectively utilize PU’s signal, both energy harvesting and information can be transferred between PU and SU via simultaneous wireless and information power transfer. Our primary objective is to study the performance analysis of WEH for bidirectional communication in the CR network in this research.

1.1.2 Power splitting technique

Liu et al. presented a multiple spectrum sensing and EH framework model where the sensing slot is divided into various sensing and EH sub-slots. The joint optimization problem has been discussed for increasing the throughput of SU detecting the false alarm conditions [16]. Son et al. conducted studies to measure the performance of power splitting ratio, and power-sharing coefficient in PU and SU in CR network [17]. In [18], authors explored channel capacity, transmission probability, optimal transmission power to maximizes EH, and spectrum sensing in the CR network. The work in [19] enhanced the energy harvesting of transmitted signal of antennas by selecting the optimal value of power splitting factor for energy harvesting, information transfer, and blocked signal
probability. Furthermore, the outage problem is also derived for MISO and single-input multiple-output (SIMO) technique to examine physical layer security for both models.

1.1.3 Both time and power splitting techniques
Ghosh et al. presented a comparative analysis of one-way and bidirectional communication on RF-EH relay in CR networks [20]. The experiment results indicate that hybrid power time-switching relaying (HPTSR) performs better than power splitting relay (PSR) around 35%. In [21], Sabuj and Hamamura illustrated the performance of RF energy harvesting in a random CR network where transmitter and receiver are deployed randomly. It is has been shown that outage probability is inversely proportional with transmission power, and harvested DC power improves with higher transmission power. They recommended RF-EH model as a good alternative for the longevity of wired battery devices. The authors in [22] studied particle swarm optimization algorithm for EH-based hybrid SWIPT CR network with bidirectional communication. Their primary objective was to increase the total system throughput and maximum energy efficiency of the network. Furthermore, in [23], authors studied the energy efficiency optimization model for bidirectional energy harvesting sensor networks. They introduced fractional programming and alternative search methods to achieve high transmission power and resolve the power constraint problem of relay and sensor nodes.

1.2 Scope and contributions
In the previously mentioned literature in [20], the work investigated the minimum outage probability. However, this paper investigates the energy efficiency of EH in CR for bidirectional communication. An EH-based CR network model is introduced here where SU can simultaneously transfer information and harvest energy from PU during assigned time slots. The significant contribution of this paper is presented as follows:

- This paper introduces an EH-based CR network model for bidirectional communication between mobile user equipment (MUE) and base station (BS) for simultaneous information and energy transfer. The achievable data rate between BS and MUE for both uplink and downlink scenarios is studied here.
- We also derive the outage probability and energy efficiency of the existing CR network for uplink and downlink communication systems.
- Furthermore, we derive the optimal transmission power and energy harvesting power expressions for maximum energy efficiency in a given CR network.
- Finally, the numerical results provide a practical guideline that the proposed bidirectional EH-based CR network model can significantly improve the highlighted existing problems by various system parameters, such as transmission power of BS, harvested power, and distance between MUE and BS. The simulation results also reveal that the energy efficiency of the proposed scheme is significantly improved compared to optimal transmission power and energy harvesting power.
Table 1: Summary of symbols for downlink and uplink

| Description                              | Symbol | Description                              | Symbol |
|------------------------------------------|--------|------------------------------------------|--------|
| Transmission power of BS                | $P_{BS}$ | Transmission power of MUE                | $P - P_s$ |
| Transmit signal of BS                   | $x_{BS}$ | Transmit signal of MUE                   | $x_{MUE}$ |
| Channel gain from BS $\rightarrow$ MUE  | $g_{BS}$ | Channel gain from MUE $\rightarrow$ BS   | $g_{MUE}$ |
| Transmission power of PT                | $P_p$  | Transmit signal of PT                    | $x_p$  |
| Distance from PT $\Rightarrow$ MUE     | $d_p$  | Distance from PT $\Rightarrow$ BS       | $d_i$  |
| Distance from BS $\Rightarrow$ MUE     | $d_i$  | Distance from BS $\Rightarrow$ MUE      | $d_i$  |
| Channel gain between PT $\Rightarrow$ MUE | $h_{p1}$ | Channel gain between PT $\Rightarrow$ BS | $h_{p2}$ |
| Antenna noise at MUE                    | $n_{a1}$ | Antenna noise at BS                      | $n_{a2}$ |
| Baseband conversion noise               | $n_{\text{conv}}$ | Pathloss exponent                      | $\alpha$ |
| Time allocation factor                  | $\tau$ | Constant harvesting power               | $P$    |
| Circuit power consumption of BS         | $P_{\text{cir}}$ | Circuit power consumption of MUE         | $P_{\text{cir}}$ |

Symbols and their short description are presented in Table 1 to understand the paper easily. The remainder of this paper is organized as follows. Section 2 presents our proposed CR network model. Section 3 obtains the theoretical expression of our proposed model’s data rate, outage probability, and energy efficiency. Also, maximum energy efficiency is discussed for uplink and downlink scenarios. Numerical results are discussed in Sect. 4. Finally, Sect. 5 concludes the paper.

2 Design and modeling of network architecture and assumptions

2.1 Network model

A CR network shown in Figure 1 is a graphical representation of bidirectional communication system between mobile user equipment (MUE)\(^1\) and base station (BS[1]) with the

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\(^1\) MUE and BS are secondary nodes to utilize the unlicensed band.
presence of primary transmitter (PT). In the downlink scenario, BS communicates with MUE. In the uplink scenario, MUE communicates with BS. It is also assumed that MUE is capable of harvesting energy from radio signals transmitted from BS. Both MUE and BS are equipped with a single transceiver for sending and receiving data.

### 2.2 Time-slot and sensing

Figure 2 is a frame structure of information and energy transfer between MUE and BS. It can be observed that for one frame duration, time slot \( T \) is separated into three parts according to time-switching method: \( \tau_1 T \), \( \tau_2 T \) and \( (1 - \tau_1 - \tau_2) T \), where \( 0 \leq (\tau_1 + \tau_2) \leq 1 \). During the first transmission phase, BS transmits its signal to MUE during \( \tau_1 T \) period. Subsequently, in second phase, spectrum sensing\(^2\) is applied over \( \tau_2 T \) period at the MUE. It is assumed that during \( \tau_1 T \), a constant power \( P \) is used for energy harvesting from BS to MUE and remaining \( P_{MUE} - P \) power is used for information transfer from BS to MUE according to power-splitting method \([21, 26]\). And in the last phase, information is sent from MUE to BS during \( (1 - \tau_1 - \tau_2) T \) period.

### 2.3 Channel model

In the considered CR network, the presence of fading channel model is acknowledged here. Due to all links, fading coefficients are assumed as independent identical random variables with zero mean and unit variance (i.e. \( g_{MUE} \sim \mathcal{CN}(0,1) \), \( g_{BS} \sim \mathcal{CN}(0,1) \), \( h_{p1} \sim \mathcal{CN}(0,1) \) and \( h_{p2} \sim \mathcal{CN}(0,1) \)). Here, the symbol \( g_{MUE} \) and \( g_{BS} \) refer to the fading coefficient link from MUE to BS and the fading coefficient link from BS to MUE. Also, the symbol \( h_{p1} \) and \( h_{p2} \) refer to the fading coefficient link from PT to MUE and the fading coefficient link from PT to BS.

### 3 Mathematical modeling and definition

#### 3.1 Definition of metric

##### 3.1.1 Data rate

Data rate can be defined as the speed at which information is transferred between MUE and BS or vice versa in CR network.

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\(^2\) Sensing is a fundamental aspect in CR networks, otherwise it causes interference with the PT \([24, 25]\).
3.1.2 Outage probability

Outage probability can be described as probability of received signal-to-interference-plus-noise ratio (SINR) at any given node is lower than the predefined threshold for that particular receiver.

3.1.3 Energy efficiency

Energy efficiency is the ratio between successful data rate to transmission power and total circuit power consumption in a device (e.g. MUE and BS).

3.2 Downlink scenario

Signal received for transmitting information and energy harvesting at MUE from BS can be denoted as

\[ y_{\text{MUE}} = \sqrt{P_{\text{BS}} g_{\text{BS}} x_{\text{BS}}} \sqrt{(d_s)^\alpha} + \sqrt{P_p h_{\text{PT}} x_p} \sqrt{(d_p)^\alpha} + n_{\text{a1}} + n_{\text{conv}} \]  (1)

where \( P_{\text{BS}} \) denotes the transmission power of BS, \( g_{\text{BS}} \) is the channel gain from BS to MUE, \( x_{\text{BS}} \) represents transmit signal of BS with zero mean and \( \text{E}[|x_{\text{BS}}|^2] = 1 \), \( d_s \) is the distance between BS and MUE, \( P_p \) is transmission power of PT, \( d_p \) denotes the distance from PT to MUE, \( h_{\text{PT}} \) is channel gain between PT to MUE, \( x_p \) is transmit signal of PT with zero mean and \( \text{E}[|x_p|^2] = 1 \), \( n_{\text{a1}} \) and \( n_{\text{conv}} \) represents antenna noise for signal transmission from BS to MUE and baseband conversion noise, respectively.

Subsequently, received signal power at MUE from BS using Eq. (1) can be calculated as:

\[ P_{\text{MUE}} = \frac{\Psi_1 P_{\text{BS}} (g_{\text{BS}})^2}{d_s^2} \]  (2)

where \( 0 < \Psi_1 \leq 1 \) denotes the energy conversion efficiency of radio signal-to-power depending on the harvesting circuitry.

During \( \tau_1 T \) period, the received power from BS is divided into two parts: continuous power \( P \) is used for energy harvesting and remaining power \( (P_{\text{MUE}} - P) \) is used for information transfer from BS to MUE according to power-splitting method [21, 26]. Accordingly, SINR at MUE from BS can be defined as

\[ \gamma_{\text{MUE}} = \frac{P_{\text{MUE}} - P}{\sigma_i^2 + \frac{P_p h_{\text{PT}}}{(d_p)^\alpha}} \]  (3)

where \( \sigma_i^2 \) is denoted as \( \sigma_i^2 = \sigma_{\text{a1}}^2 + \sigma_{\text{conv}}^2 \).

From Eq. (3), data rate from BS to MUE can be defined as

\[ R_{\text{MUE}} = \frac{\tau_1 T}{T} \log_2(1 + \gamma_{\text{MUE}}) = \tau_1 \log_2(1 + \gamma_{\text{MUE}}) \]  (4)

From Eq. (4), outage probability from BS to MUE can be derived as follows
\[ OP_{\text{MUE}} = P_r \left[ r_1 \log_2(1 + \gamma_{\text{MUE}}) < R_1 \right] \]
\[ = 1 - P_r \left[ r_1 \log_2(1 + \gamma_{\text{MUE}}) > R_1 \right] \]
\[ = 1 - P_r \left[ \gamma_{\text{MUE}} > 2^{R_1} - 1 \right] \]
\[ = 1 - P_r \left( \frac{P_{\text{MUE}} - P}{\sigma^2 + P_{\text{BS}} h \sigma^2} > 2^{R_1} - 1 \right) \]
\[ = 1 - P_r \left[ P_{\text{MUE}} > (2^{R_1} - 1)\left(\sigma^2 + P_{\text{BS}} h \sigma_p^2\right) + P \right] \]
\[ = 1 - P_r \left( g_{\text{BS}}^2 > \frac{\left(2^{R_1} - 1\right) \left(\sigma^2 + P_{\text{BS}} h \sigma_p^2\right) + P}{\Psi_1 P_{\text{BS}}} \right) \]
\[ = 1 - \exp \left( - \frac{\left(2^{R_1} - 1\right) \left(\sigma^2 + P_{\text{BS}} h \sigma_p^2\right) + P}{\Psi_1 P_{\text{BS}}} \right) \]

where \( R_1 \) is defined as the target data rate. Energy efficiency of BS can be expressed as

\[ EE_{\text{BS}} = \frac{R_{\text{MUE}}}{P_{\text{cir}}^{\text{BS}} + P_{\text{BS}}} \]  

### 3.3 Maximum energy efficiency in downlink

To find the optimal transmission power in terms of energy efficiency, we set the derivative of Eq. (6) with respect to \( P_{\text{BS}} \) equal to zero leading to

\[ P_{\text{BS}}^* = \arg_{P_{\text{BS}}} \left\{ \frac{dEE_{\text{BS}}(P_{\text{BS}})}{dP_{\text{BS}}} = 0 \right\} \]  

By taking the first-order derivative of Eq. (6) with respect to \( P_{\text{BS}} \), we get:

\[
\frac{dEE_{\text{BS}}}{dP_{\text{BS}}} = 0
\]
\[
\text{or, } \frac{\log(1 - a)}{P_{\text{BS}} + P_{\text{BS}}^{\text{cir}}} = \frac{g_{\text{BS}}^2}{(d_i)^a(a - 1)q}
\]
\[
\text{or, log}(1 - a)(1 - a) = \frac{g_{\text{BS}}^2(P_{\text{BS}} + P_{\text{BS}}^{\text{cir}})}{(d_i)^a q}
\]
\[
\text{or, log}(1 - a) \left( 1 - \frac{P - \Psi_1 P_{\text{BS}} g_{\text{BS}}^2}{\Psi_1 P_{\text{BS}} g_{\text{BS}}^2} \right) q = \frac{g_{\text{BS}}^2(P_{\text{BS}} + P_{\text{BS}}^{\text{cir}})}{(d_i)^a}
\]
\[
\text{or, log}(1 - a) \left( q - \left( P - \Psi_1 P_{\text{BS}} g_{\text{BS}}^2 \right)(d_i)^a \right) = \frac{g_{\text{BS}}^2(P_{\text{BS}} + P_{\text{BS}}^{\text{cir}})}{(d_i)^a}
\]
\[
\text{or, log}(1 - a) \left( \Psi_1 P_{\text{BS}} g_{\text{BS}}^2 + (d_i)^a q - P(d_i)^a \right) = g_{\text{BS}}^2(P_{\text{BS}} + P_{\text{BS}}^{\text{cir}})
\]
\[
\text{or, log}(1 - a) = \frac{g_{\text{BS}}^2(P_{\text{BS}} + P_{\text{BS}}^{\text{cir}})}{\Psi_1 P_{\text{BS}} g_{\text{BS}}^2 + (d_i)^a q - P}
\]
\[
\text{or, log}(1 - a) = 1 - \frac{g_{\text{BS}}^2(P_{\text{BS}} + P_{\text{BS}}^{\text{cir}})}{\Psi_1 P_{\text{BS}} g_{\text{BS}}^2 + (d_i)^a q - P} - 1
\]
\[
\text{or, } \frac{\Psi_1 P_{\text{BS}} g_{\text{BS}}^2 + (d_i)^a q - P}{(d_i)^a q} e^{-1} = \exp \left( \frac{\left(1 - \Psi_1 P_{\text{BS}} g_{\text{BS}}^2 + g_{\text{BS}}^2 P_{\text{BS}}^{\text{cir}} - (d_i)^a q - P \right)}{\Psi_1 P_{\text{BS}} g_{\text{BS}}^2 + (d_i)^a q - P} \right)
\]

where \( a \) denotes \( a = \frac{P - \Psi_1 P_{\text{BS}} g_{\text{BS}}^2}{\sigma^2 + P_{\text{BS}} h \sigma_p^2} \) and \( q \) indicates \( q = \sigma^2 + P_{\text{BS}} h \sigma_p^2 \).
By applying Lambert method in Eq. (8), we can write

\[ W(\beta_1) = \frac{(1 - \Psi_1) P_{BS} g_{BS}^2 + g_{cir}^2 P_{BS} - (d_s)^a (q - P)}{\Psi_1 P_{BS} g_{BS}^2 + (d_s)^a (q - P)} \]

or,

\[ 1 + W(\beta_1) = 1 + \frac{(1 - \Psi_1) P_{BS} g_{BS}^2 + g_{cir}^2 P_{BS} - (d_s)^a (q - P)}{\Psi_1 P_{BS} g_{BS}^2 + (d_s)^a (q - P)} \]

\[ \text{or}, 1 + W(\beta_1) = \frac{P_{BS} g_{BS}^2 + g_{cir}^2 P_{BS}}{\Psi_1 P_{BS} g_{BS}^2 + (d_s)^a (q - P)} \]

\[ \text{or}, [\Psi_1 P_{BS} g_{BS}^2 + (d_s)^a (q - P)] [1 + W(\beta_1)] = g_{BS}^2 P_{BS} + g_{cir}^2 P_{BS} \]

\[ \text{or}, \Psi_1 P_{BS} g_{BS}^2 [1 + W(\beta_1)] - P_{BS} g_{cir}^2 = g_{cir}^2 P_{BS} - (d_s)^a (q - P) [1 + W(\beta_1)] \]

where \( \beta_1 = \frac{\Psi_1 P_{BS} g_{BS}^2 + (d_s)^a (q - P)}{(d_s)^q} e^{-1} \) and \( W(\cdot) \) is Lambert function.

Finally, after some mathematical manipulation in Eq. (9), \( P_{BS} \) can be written as

\[ P_{BS}^* = \frac{g_{cir}^2 P_{BS} - (d_s)^a (q - P) [1 + W(\beta_1)]}{g_{BS}^2 (\Psi_1 [1 + W(\beta_1)] - 1)} \]  \hspace{1cm} (10)

One can see that Eq. (10) depends on Lambert function \( W(\beta_1) \). \( W(\beta_1) \) has exactly one real solution for all real \( \beta_1 \geq 0 \). \( W(\beta_1) \) has exactly two real solutions for \( -e^{-1} < \beta_1 < 0 \), where the larger solution is considered for the upper bound of optimal power and the smaller solution is considered for the lower bound of optimal power [27]. In Eq. (10), optimal transmission power increases with \( d_s \), so \( P_{BS}^* \) can be expressed as

\[ P_{BS}^* = \min \left\{ \frac{g_{cir}^2 P_{BS} - (d_s)^a (q - P) [1 + W(\beta_1)]}{g_{BS}^2 (\Psi_1 [1 + W(\beta_1)] - 1)}, P_{BST} \right\} \]  \hspace{1cm} (11)

where \( P_{BST} \) is the total power budget of BS. For the maximum energy efficiency, we put \( P_{BS}^* \) in Eq. (6).

### 3.4 Uplink scenario

Signal received at BS\(^3 \) from MUE can be written as

\[ y_{BS} = \sqrt{\frac{P - P_{dMUE} x_{MUE}}{d_s^2}} + \sqrt{\frac{P_{P_2} h_{P_2} x_p}{d_s^2}} + n_{a_2} + n_{conv} \]  \hspace{1cm} (12)

where \( P - P_3 \) denotes the transmission power of signal carrying information from MUE to BS, where \( P_3 \) represents the spectrum sensing power. \( g_{MUE} \) is the channel gain from MUE to BS, \( x_{MUE} \) represents transmit signal of MUE with zero mean and \( E[|x_{MUE}|^2] = 1 \), \( d_s \) is the distance between BS and MUE, \( P_p \) is transmission power of PT, \( d_k \) denotes the distance from PT to BS, \( h_{P_2} \) is channel gain between PT to BS, \( x_p \) is transmit signal of PT with zero mean and \( E[|x_p|^2] = 1 \), \( n_{a_2} \) and \( n_{conv} \) represent antenna noise for signal transmission from BS to MUE and baseband conversion noise, respectively.

\(^3 \) To simplify design, we assume one MUE. For the multiple active MUEs, BS is equipped with the massive multiple-input and multiple-output (M-MIMO) antenna. M-MIMO is one of the advanced technology of MIMO, having several antennas at BS to serve multiple active MUEs [28].
Similarly, received signal power at BS from MUE using Eq. (12) can be calculated as

\[ P_{BS} = \frac{\Psi_2(P - P_s)(g_{\text{MUE}})^2}{d_s^\alpha} \]  \hspace{1cm} (13)

where \( 0 < \Psi_2 \leq 1 \) denotes the energy conversion efficiency.

Consequently, SINR at BS from MUE can be obtained as

\[ \gamma_{BS} = \frac{P_{BS}}{\sigma_s^2 + \frac{P_h g_{\text{MUE}}}{d_k} d^\alpha} \]  \hspace{1cm} (14)

Furthermore, data rate between MUE and BS from Eq. (14) can be defined as

\[ R_{BS} = \frac{(1 - \tau_1 - \tau_2)T}{T} \log_2(1 + \gamma_{BS}) = (1 - \tau_1 - \tau_2) \log_2(1 + \gamma_{BS}) \]  \hspace{1cm} (15)

From Eq. (15), outage probability from MUE to BS can be derived as follows

\[ OP_{BS} = P_r[(1 - \tau_1 - \tau_2) \log_2 (1 + \gamma_{BS}) < R_2]\]

\[ = 1 - P_r[(1 - \tau_1 - \tau_2) \log_2 (1 + \gamma_{BS}) > R_2]\]

\[ = 1 - P_r \left[ \gamma_{BS} < \frac{1}{2(1 - \tau_1 - \tau_2)} - 1 \right] \]

\[ = 1 - P_r \left[ \frac{P_{BS}}{\sigma_s^2 + \frac{P_h g_{\text{MUE}}}{d_k} d^\alpha} > \frac{1}{2(1 - \tau_1 - \tau_2)} - 1 \right] \]

\[ = 1 - P_r \left[ P_{BS} > \frac{1}{2(1 - \tau_1 - \tau_2)}(\sigma_s^2 + P_h g_{\text{MUE}} d_k^{-\alpha}) \right] \]

\[ = 1 - P_r \left[ \frac{\Psi_2(P - P_s)(g_{\text{MUE}})^2}{d_s^\alpha} > \frac{1}{2(1 - \tau_1 - \tau_2)}(\sigma_s^2 + P_h g_{\text{MUE}} d_k^{-\alpha}) \right] \]

\[ = 1 - \exp \left( -\frac{1}{\Psi_2(P - P_s)} \frac{(\sigma_s^2 + P_h g_{\text{MUE}} d_k^{-\alpha})}{d_s^\alpha} \right) \]  \hspace{1cm} (16)

where \( R_2 \) is threshold data rate. Energy efficiency of MUE can be expressed as

\[ EE_{\text{MUE}} = \frac{R_{BS}}{P_{\text{cir}}^{\text{MUE}} + P - P_s} \]  \hspace{1cm} (17)

### 3.5 Maximum energy efficiency in uplink

To find constant power in terms of energy efficiency, we set the derivative of Eq. (17) with respect to \( P \) equal to zero leading to
\[ P^* = \arg_{P} \left\{ \frac{dEE_{MUE}(P)}{dP} = 0 \right\} \] (18)

By taking the first-order derivative of Eq. (17), we get
\[
\frac{dEE_{MUE}}{dP} = 0
\]
or,\[
\log(b) = \frac{g_{MUE}^2 (P + p_{MUE} - P_s)}{by(d_s)\alpha}
\]
or, \[
\log(b) = \frac{\frac{g_{MUE}^2}{(d_s)\alpha} y (\frac{\psi_2(P - P_s)g_{MUE}^2 y}{(d_s)\alpha})^2 - y(d_s)\alpha}{(d_s)\alpha y}
\]
or, \[
\frac{\frac{\psi_2(P - P_s)g_{MUE}^2 y}{(d_s)\alpha} + (d_s)\alpha y}{(d_s)\alpha y} e^{-1} = e^c
\]
where \( b \) is defined as \( b = 1 + \frac{\psi_2(P - P_s)g_{MUE}^2 y}{(d_s)\alpha} \) and \( y \) is calculated as \( y = \sigma^2 + \frac{P_w b}{d_s}\alpha \) and \( c = \frac{(1 - \psi_2(P - P_s)g_{MUE}^2 y)}{\psi_2(P - P_s)g_{MUE}^2 y(d_s)\alpha} \).

By applying Lambert method in Eq. (19), we can write
\[
W(\beta_2) = \frac{(1 - \psi_2(P - P_s)g_{MUE}^2 y)}{\psi_2(P - P_s)g_{MUE}^2 y(d_s)\alpha} - y(d_s)\alpha
\]
or, \[
1 + W(\beta_2) = \frac{(1 - \psi_2(P - P_s)g_{MUE}^2 y)}{\psi_2(P - P_s)g_{MUE}^2 y(d_s)\alpha} + y(d_s)\alpha
\]
or, \[
1 + W(\beta_2) = \frac{(P - P_s)g_{MUE}^2 + g_{MUE}^2 p_{MUE}^\text{MUE} y(d_s)\alpha}{\psi_2(P - P_s)g_{MUE}^2 + y(d_s)\alpha}
\]
where \( \beta_2 = \frac{(1 - \psi_2(P - P_s)g_{MUE}^2 y)}{\psi_2(P - P_s)g_{MUE}^2 y(d_s)\alpha} - e^{-1} \).

Finally, after some mathematical manipulation in Eq. (20), \( P^* \) can be expressed as
\[
P^* = \frac{g_{MUE}^2 p_{MUE}^\text{MUE} y(d_s)\alpha [1 + W(\beta_2)]}{g_{MUE}^2 (1 + W(\beta_2)) - 1} + P_s
\] (21)

One can see that Eq. (21) depends on Lambert function \( W(\beta_2) \). \( W(\beta_2) \) has exactly one real solution for all real \( \beta_2 \geq 0 \). \( W(\beta_2) \) has exactly two real solutions for \(-e^{-1} < \beta_2 < 0\), where the larger solution is considered for the upper bound of optimal power and the smaller solution is considered for the lower bound of optimal power [27]. In Eq. (21), optimal harvested power increases with \( d_s \), so \( P \) can be expressed as
where $P_M$ is the maximum harvested power. For the maximum energy efficiency, we put $P^\star$ in Eq. (17).

4 Simulation results and discussion

The performance in terms of data rate, outage probability, energy efficiency, and optimization technique is evaluated in this section. Some parameters are changed depending on the figure which is mention in the figure. All simulations are executed by considering $\alpha = 4, \tau_1 = 0.4, \tau_2 = 0.2, \Psi_1 = 0.65, \Psi_2 = 0.65, R_1 = 1, R_2 = 1, d_p = 1800$ m, $d_k = 2000$ m, $d_s = 100$ m, $P_p = 120$ dBm, $P_{\text{cir}}^{\text{BS}} = 120$ W, $P_{\text{MUE}}^{\text{cir}} = 1$ W, and $\sigma_s^2 = -174$ dBm. Monte Carlo simulations are run over 10,000 times for the different fading coefficients.

4.1 Downlink analysis

4.1.1 Data rate

Figure 3 shows that data rate is a monotonically increasing function of transmission power. Data rate shows an abysmal performance almost close to zero up to 5 dBm transmission power. After that, with increasing transmission power, data rates take a sharp rise and reach the maximum value of 3.367 bps/Hz at 40 dBm transmission power for $P = 0.5 \times P_{\text{MUE}}$. As transmission power increases, more power is assigned for information transfer between BS and MUE. We can observe an improvement of 90.12% in data rate for varying the transmission power from 25 dBm to 35 dBm for $P = 0.5 \times P_{\text{MUE}}$. Compared between $P = 0.2 \times P_{\text{MUE}}$ and $P = 0.5 \times P_{\text{MUE}}$, $P = 0.2 \times P_{\text{MUE}}$ is better because of more power $(P_{\text{MUE}} - P)$ is allocated for information transfer. The theoretical and simulation results are compared in Fig. 3. The simulation result is fairly close to the theoretical result, which validates in Eq. (4).

$$P^\star = \min \left\{ \frac{g_{\text{MUE}}^2 P_{\text{MUE}}^{\text{cir}} - y(d_s)^\alpha [1 + W(\beta_2)]}{g_{\text{MUE}}^2 (\Psi_2 [1 + W(\beta_2)] - 1)} + P_s, P_M \right\}$$

(22)
Figure 4 represents the comparative analysis of data rate versus distance between BS and MUE. It is observed that the data rate continues to drop gradually for the increasing distance between BS and MUE for downlink communication. The figure shows that the maximum achievable data rate is 12.93 bps/Hz when the distance is almost zero between BS and MUE. This can be explained by the fact that as distance increases between BS and MUE, the SINR of the downlink system gets worse. For a variation of 100 m to 150 m, we notice a decrease of 2.313 bps/Hz to 1.418 bps/Hz which is 38.69% decrease for $P = 0.5 \times P_{MUE}$ in data rate.

4.1.2 Outage probability
Figure 5 describes the performance of outage probability for different values of transmission power. Initially, the outage probability of the system for downlink communication stays constant at its peak value of 1 and then drops quickly as the transmission power
increase in the range of $10 - 40$ dBm for both the curves. $P = 0.2 \times P_{\text{MUE}}$ is lower outage probability in comparison with $P = 0.5 \times P_{\text{MUE}}$. This is because more power is allocated for information transfer in $P = 0.2 \times P_{\text{MUE}}$. As a result, SINR will rise, which eventually results in a low outage probability. The simulation result is fairly close to the theoretical result, which validates in Eq. (5).

The result of the outage probability concerning the distance between BS and MUE is shown in Fig. 6. Here, we can observe that outage probability is steadily increasing with increasing distance. The explanation here is that when distance is less between BS and MUE, the path loss is low between BS and MUE during downlink communication. It can be seen that $P = 0.2 \times P_{\text{MUE}}$ shows a lower outage performance decrease of 18.10% in comparison with $P = 0.5 \times P_{\text{MUE}}$ for a distance of 200 m between BS and MUE.
4.1.3 Energy efficiency

Figure 7 exhibits the energy efficiency of our given system of bidirectional communication versus transmission power. Here, we can observe that the energy efficiency rises with increasing transmission power and reaches the optimal value of 0.0279 bps/Hz/W and 0.0257 bps/Hz/W for $P = 0.2 \times P_{ \text{MUE}}$ dBm and $P = 0.5 \times P_{ \text{MUE}}$ dBm, respectively. It can be further observed that $P = 0.2 \times P_{ \text{MUE}}$ dBm shows better performance in terms of energy efficiency than $P = 0.5 \times P_{ \text{MUE}}$ dBm. For consideration of $P_{ \text{BS}} = 30$ dBm, there is 13.32% increase in energy efficiency for $P = 0.2 \times P_{ \text{MUE}}$ dBm. The explanation here is that when $P$ is low and $P_{ \text{MUE}} - P$ is high, so the data rate and energy efficiency are high based on Eq. (6).

Figure 8 illustrates the performance of energy efficiency for transmitting power for both original and optimal graphs based on Eqs. (6) and (11). From the figure, it is clear that the optimal curve remains a constant value of 0.2855 bps/Hz/W for various transmission

![Energy efficiency vs. transmission power of BS comparison in downlink](image1)

![Energy efficiency vs. distance from BS to MUE in downlink](image2)
power. However, the original curve rises gradually with increasing transmission power and reaches the maximum 0.2798 bps/Hz/W at 40 dBm. There is an improvement of 48.95% in terms of energy efficiency in the optimal curve than the original for 30 dBm power.

Figure 9 shows the effect of energy efficiency for distance for the downlink communication. From the figure, we can observe that both curves were linearly decreasing with respect to distance. However, $P = 0.2 \times P_{MUE}$ curve shows better performance in terms of energy efficiency. For example, $P = 0.2 \times P_{MUE}$ is an improvement of 6.85% compared with $P = 0.5 \times P_{MUE}$ for 50 m distance between BS and MUE.

Figure 10 displays the energy efficiency versus distance for downlink communication in a bidirectional communication system for original and optimal curves based on (6) and (11). As we can observe from the figure, the optimal curve gradually decreases as a distance function and reaches a minimum value of 0.01276 bps/Hz/W at 300 m distance. Similarly, the original curve shows the minimum value of 0.003449 at 300 m. For a variation of 100 m to 150 m, we observe a decrease of 35.24% for the original curve and subsequently 20.53% decrease for the optimal curve. The performance of the optimal curve is better than the original curve in the simulation because of transmission power based on (11) which ultimately leads to an increase in energy efficiency.

4.2 Uplink analysis

4.2.1 Data rate

Figure 11 shows that data rate is a monotonically increasing function of harvested power. Data rate shows an abysmal performance almost close to zero up to 5 dBm harvested power. After that, with increasing, harvested power data rate takes a sharp rise and reaches the maximum value of 2.29 bps/Hz and 2.51 bps/Hz at 30 dBm harvesting power for $P_s = 0.5 \times P$ and $P_s = 0.2 \times P$, respectively. We can observe an improvement of 85.84% in data rate for varying the harvesting power from 15 dBm to 20 dBm for $P_s = 0.5 \times P$. This is because $P_s$ is low and $P - P_s$ is high. Thus, it improves the data rate. Moreover, the theoretical result exactly matches the simulation result.
Figure 12 represents the comparative analysis of data rate versus distance between BS and MUE. It is observed that the data rate continues to drop gradually for the increasing distance between BS and MUE for uplink communication. The figure shows that the maximum achievable data rate is 12.93 bps/Hz when the distance is almost zero between MUE and BS. This can be explained by the fact that as distance increases between BS and MUE, the SINR of the uplink system gets worse. Thus, the data rate tends to drop between BS and MUE. For a variation of 100 m to 150 m, we notice a decrease of 38.97% for $P_s = 0.5 \times P$ in terms of data rate.

4.2.2 Outage probability

Figure 13 describe the performance of system outage for different value of harvested power. Initially, the outage probability of the system for uplink communication remains
constant and then drops quickly as the harvested power increase in the range of $11 - 30$ dBm for both the curves. Almost 5% more harvested power is needed for $P_s = 0.5 \times P$ to gain the outage probability of 0.55 in comparison with $P_s = 0.2 \times P$. Due to higher harvested power, more power is allocated for information transfer in the system. As a result, information can be transmitted easily to BS, and SINR will rise, resulting in low outage probability.

The result of outage probability against the distance between BS and MUE is shown in Fig. 14. Here, we can observe that outage probability increases with increasing distance. This is because the path loss is low for a short distance. For $P_s = 0.5 \times P$, outage probability reaches the maximum value of 1 at 260 m and when $P_s = 0.2 \times P$, outage probability gets it maximum value of 1 at 280 m. Because, $P_s$ is low where as the $P - P_s$ is high, so it covers more distance.
4.2.3 Energy efficiency

Figure 15 depicts the performance of energy efficiency with respect to harvested power in the bidirectional system for uplink communication. From the figure, it can be observed that energy efficiency increases with increasing harvested power. As harvested power increases and reaches the maximum value of 0.4651 bps/Hz/W and 0.4411 bps/Hz/W at 30 dBm for $P_s = 0.5 \times P$ and $P_s = 0.2 \times P$, respectively. This is because $P_s$ is high and $P - P_s$ is low. Therefore, $P - P_s$ increases, the energy efficiency decreases based on Eq. (17). In addition, the theoretical result exactly matches the simulation result.

Regarding Fig. 15, Fig. 16 presents the effect of energy efficiency with varying harvesting power and performance comparison also shown between original and optimal curve based on (17) and (22). The figure shows that the optimal curve, an extended version of (17), remains a constant value of 0.440 bps/Hz/W for various harvested power. However, the original curve rises gradually with increasing harvesting power and reaches the
maximum value of 0.440 bps/Hz/W, which matches the optimal value at 30 dBm. This is because maximum power is allocated for data transmission at 30 dBm. For a variation of 15 dBm to 20 dBm harvested power, the original curve shows an improvement of 71.23%.

Figure 17 represents the energy efficiency of the given system for uplink communication with respect to various distances. The figure shows that the energy efficiency continues to fall with increasing distance between BS and MUE. For a distance of 50 m, we can see an improvement of 19.98% for $P_s = 0.5 \times P$ in comparison with $P_s = 0.2 \times P$. $P_s = 0.5 \times P$ is higher energy efficiency in comparison with $P_s = 0.2 \times P$. This is because $P_s$ is high and $P - P_s$ is low. Therefore, $P - P_s$ increases, the energy efficiency decreases based on Eq. (17). For the high distance between BS and MUE, the data rate drops significantly for information transfer as the necessary power allocated for information
transfer is lower than the predetermined threshold limit. For decreasing data rates, the energy efficiency of a given system will also drop.

Figure 18 exhibits a performance comparison between original and optimal curve for energy efficiency versus distance for the uplink communication system. We can observe that both curves decrease for distance. The optimal curve shows better performance in terms of energy efficiency of 19.15% increase for 50 m distance between BS and MUE. However, original and optimal performance are the same after 126 m. This is because maximum harvested power is allocated for data transmission based on (22) at 126 m and then is allocated the same power for both scheme. Performance of optimal curve is better than the original curve in the simulation because the variation of harvested power based on (20) which ultimately leads to increase in energy efficiency [29, 30].

5 Conclusion and future works

Energy harvesting from RF signals is now considered a promising new solution for the longevity of battery life in traditional wireless devices. This paper introduces a WEH technique based on the CR network for bidirectional communication. The mathematical expression of data rate, outage probability, and energy efficiency for downlink and uplink scenarios is presented here. In addition, maximum energy efficiency is obtained for optimal transmission power and energy harvesting power in downlink and uplink scenarios. Numerical results show better performance of energy efficiency using optimal transmission power in a downlink scenario. Also, energy efficiency performance is improved using optimal energy harvesting power in the uplink scenario. The study can be extended for some future research like transmit antenna selection technique [29], two-slope path loss [21], truncated channel inversion power control [30], and secure CR network [31]. In addition, we calculate the energy efficiency of the whole network for the proposed scheme.

Abbreviations
AI: Artificial Intelligence; BS: Base station; CR: Cognitive radio; DC: Direct current; EH: Energy harvesting; HPTSR: Hybrid power time switching relaying; IOT: Internet of Things; MAC: Media access control; MUE: Mobile user equipment; PU: Primary users; PSR: Power splitting relay; PT: Primary transmitter; RF: Radio frequencies; SU: Secondary users; WEH: Wireless energy harvesting.

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Declarations

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Competing interests
The authors declare that they have no competing interests.

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