Conflict-free routing of multi-stop warehouse trucks

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Abstract
The recent interest in greater vehicular autonomy for factory and warehouse automation has stimulated research in conflict-free routing: a challenging network routing problem in which vehicles may not pass each other. Motivated by a real-world case study, we consider one such application: truck movements in a tightly constrained warehouse. We propose an extension of an existing conflict-free routing algorithm to consider multiple stopping points per route. A high level metaheuristic is applied to determine the route construction and assignment of vehicles to routes.

Keywords Conflict-free routing · Shortest path · Metaheuristic · Graphs · Permutations

1 Introduction
Conflict-free routing appears in many applications where routes are constrained to the extent that vehicles may not pass each other without taking alternative routes. Previous application areas have included scheduling multiple cranes in steel logistics, transportation of containers with automated guided vehicles (AGVs), routing of taxiing aircraft and movements of trains. The motivating problem for the proposed approach is the allocation of routes to trucks in a warehouse, such routes being numbered in thousands per day. Each truck can carry multiple items that must be retrieved from various locations. Given the tight alleyways in which the trucks manoeuvre, the efficient allocation of conflict-free routes in real time is crucial. Due to width constraints, the horizontal gaps between rows are one way.
Conflict-free routing approaches allocate point-to-point routes across a graph one vehicle at a time, adding diversions and waits to avoid the paths of already-routed vehicles by considering a time-expanded version of the graph. These have proved very efficient compared to the alternative approaches that compute routes (ignoring time) and retrospectively amend the routes to avoid collisions, frequently leading to deadlocks [8].

Earlier work has proposed conflict-free routing approaches based on variations of the well-known Dijkstra’s [3,17] and A* [4,16,19] shortest path algorithms. The focus in this article is on the conflict-free routing algorithm QPPTW [17], a variant of Dijkstra’s shortest path algorithm that accounts for the times of previous vehicle movements. QPPTW finds a shortest route by expanding routes from the start vertex, applying labels to each vertex that represent the shortest path to the vertex found so far. Our proposed modification adds a stack to labels, storing the required intermediate stops that have yet to be processed. When this stack is empty, the route is complete. We term this new algorithm QPPTW-m (QPPTW for multiple points).

QPPTW-m is more general than earlier works in conflict-free routing ([8,9,17] and others), which only considered allocation of routes with a single start and single end point with no required intermediate stopping points. Clearly, in the more general case the requirement exists to have intermediate points, visiting multiple points in a specified order. QPPTW-m is also accompanied by a metaheuristic to determine the order which to route the vehicles, and allocate jobs to the trucks. In subsequent sections, we present QPPTW-m and demonstrate its practical applicability.

2 Related work

Conflict-free routing appears in several application areas, including transportation of containers with automated guided vehicles (AGVs) [8,9], forklift movement[19], taxiing aircraft [1,3,17] and rail operations [5].

Approaches to these problems can be divided into two groups [8]. The first group of approaches allocate routes then retrospectively avoid deadlocks, either as part of the objective function, or though some kind of repair operation. Examples include [13,15], which used metaheuristics to allocate the routes. The second group of approaches (e.g. [3,4,16,17,19]) tend to use a variation of shortest path algorithms such as Dijkstra or A*, with an addition of a time element to only construct collision-avoiding routes. The closest to the proposed approach is Vivaldini et al. [19], in that it also includes a top-level heuristic to allocate jobs to trucks. However, all these approaches are for routes between single (origin,destination) pairs; the present work extends this to multi-point routes.

Several studies analysed system-level deadlocks and prevention in container terminals [6]. Many rely on the highly-constrained grid structure of the terminals, with routing being a search over predefined routes [11] or algorithms specific to the layout [14], rather than our general graph-based approach.

Aspects of the problem we address are shared with other well-known optimisation problems. The Travelling Salesman Problem (TSP) attempts to find the single most cost-effective path visiting specified vertices on a graph. An extension of TSP,
the Travelling Thief Problem [2], also incorporates a Knapsack Problem, whereby
the route must be chosen that also maximises the value of items collected by the
travelling vehicle. The Rich Vehicle Routing Problem [12] is also arguably a gener-
alisation of TSP, where routes are allocated to multiple vehicles. Variants of RVRP
make use of time-windows, but the distinction with those mentioned in the present
work is that with RVRP they are target times for each node, rather than times on which
edges are free for traversal. Herein lies the major difference of the present work with
TSP/RVRP: the constraint on the links, which are one-way and, crucially, one vehicle
at a time.

3 Problem

We now introduce the broader application context, then describe the specific problem
addressed by this paper and the model we adopt for its solution. Our partner company,
PostPac, provides an outsourcing warehouse service. Customers are mail order retailers
who do not wish to run their own warehouses, instead contracting PostPac to store
goods and post them out on request. This means they can benefit from economies of
scale, by mixing the storage of the different companies to best service all the requests,
and collecting a mixture of orders for a mixture of companies, to best optimise the
retrieval of goods. The issue for PostPac is how to efficiently retrieve goods in the
warehouse.

3.1 Problem description

The component of the PostPac system on which we focus is the truck based retrieval.
The task is one of time optimisation, gathering all the required items from the ware-
house in as short a period as possible. The environment is a grid based warehouse, the
basic layout of which is seen in Fig. 1. This will be developed into the directed graph
model seen in Fig. 2 obeying the following conditions:

1. There are 7 rows, each structured in the same way (see Fig. 1).
2. Each row has 56 storage points, accessible on one side only. Each storage point
has three levels.
3. Each row is split into two parts, one of 36 and one of 20 storage points, allowing
trucks to change rows at the split.
4. Each storage point contains a collection of items of different types.
5. Only the 10 trucks are allowed to move inside the system, and all can move
simultaneously. No personnel are ordinarily allowed in on foot.
6. The horizontal gaps between rows are one way, due to width constraints. The
outer border and middle avenue can be considered two way.
7. On average, there are several thousand orders to gather per day.
8. On any given journey a truck can retrieve a variety of different items, thus fulfilling
a number of orders.
9. Items are delivered by the trucks to a single collection point.
10. It is assumed that jobs have already been allocated to trucks ahead of time.
Two key issues cause inefficiency: (1) Trucks waiting on each other, due to the one way nature of the paths. This is a lack of coordination in their route planning. (2) Trucks retrieving a set of items travel all over the warehouse far more frequently than if the items for that trip were chosen more carefully.

We tackle (1) by applying a conflict-free routing algorithm to allocate routes to each truck. This finds the shortest route (in time) for trucks given a particular permutation of intermediate points for each truck, and a permutation of trucks in which to allocate their routes. This allows for automated planning of the routes, which also partially addresses (2). To fully tackle (2), we apply a metaheuristic search over these two permutation spaces to approximate the globally optimal set of routes for the trucks.

### 3.2 Model

The warehouse seen in Fig. 1 is modelled as a directed graph seen in Fig. 2, to support the one way nature of many of the paths. The storage rows are seen as the yellow vertices, a truck at one of these vertices can access materials stored at that location. Blue vertices are locations that trucks can pass through while navigating the environment but do not provide direct access to storage themselves. The red vertex is the collection point which all trucks must return to with their items. Finally the black lines represent edges, and each edge can only be used one way, due to a constraint imposed by the company. Where a route is large enough to be considered two way it is modelled as two lines of blue vertices, enabling two directions of travel.
The system contains 7 access rows, each with 56 storage points. While each storage point has 3 levels, we can ignore this as all 3 can be accessed once the truck is there (this only affects the loading time at each vertex). This gives $56 \times 7 = 392$ storage points in the system. The graph, then, has 392 vertices for accessing storage, with an additional 251 vertices for the navigation around the perimeter and central alley, and 1 vertex for the entrance/exit, to give a total of 644 vertices.

4 Proposed routing algorithm

We now focus on the core of the approach, the conflict-free routing algorithm. The order in which the stopping points are visited, and in which trucks are allocated routes, is important, but we consider this to be secondary and deal with this in Sect. 4.3. The conflict-free routing algorithm we adopt extends QPPTW, first proposed by Gawrilow et al. [9] for movements at a container terminal and later adapted for aircraft taxiing [1,3,17]. The original QPPTW allocates routes for a single start-end pair.

4.1 The existing QPPTW

Notation in the following is summarised in Table 1. The path layout is represented as a directed graph $G = (V, E)$ of vertices $V$ and edges $E$ as per Fig. 2. An edge $e \in E$ has an associated weight $\tau_e$, the estimated time to traverse $e$. Each $e$ can only have one truck $t_i$ on it at any one time. This limitation is enforced by each $e$ having an associated sorted-set of time-windows $F_e$. The $F_e$ specify the times $e$ is available for use as part of a route. A truck will only be allocated a route for which there is a chain of time-windows along its entire length, ensuring the route is conflict free. Additionally, trucks have a minimum separation equivalent to the width of one storage point at all times. This is ensured by pre-processing $G$ to find the conflicting edges $conf(e)$ for each $e$ (a conflicting edge being any edge adjacent to $e$, i.e. sharing a vertex with $e$). When a truck is routed via $e$, the time-windows of $conf(e)$ are updated to prevent other trucks conflicting with it. Long edges are divided into lengths of no more than one storage space by intermediate points to allow separation of consecutive trucks on the same path. QPPTW resembles Dijkstra’s shortest path algorithm [7], with the addition of time reservations on the edges. Vehicles are routed in sequence, with each allocated the optimal route considering already routed vehicles. By only generating routes that fit the time-windows, each route by default avoids previous routes. This means that, as long as the time-windows are updated to reflect known movements, the approach is applicable to dynamic problems. Routes can also be updated part-way through by running the routing algorithm using the current location as the starting point. However, in this article, we discuss only the static situation.

For ease of comparison, Algorithm 1 replicates QPPTW, with our new additions highlighted in blue. In the original QPPTW, the search for a shortest route is carried out by expanding the shortest path found so far from the start vertex, represented by the
Table 1  Summary of notation

| Symbol          | Description                                                                 |
|-----------------|-----------------------------------------------------------------------------|
| $G = (V, E)$    | Graph of truck paths: sets of vertices $V$ and edges $E$                     |
| $v$             | A single vertex in $V$                                                     |
| $e$             | A single edge in $E$                                                       |
| $\tau$         | A specific point in time (timestamp)                                       |
| $\tau_e$       | Weight (traversal time) for $e$                                            |
| $\tau_v$       | The loading time for vertex $v$                                            |
| $t_i$           | A single truck to be routed                                                |
| $\text{conf}(e)$ | Set of conflicting edges for $e$                                           |
| $\mathcal{F}(e)$ | Sorted set of time-windows for $e$                                         |
| $L = (v_L, I_L, \text{pred}_L, v^i_L)$ | Label on vertex $v$ for QPPTW, $\text{pred}_L$ being the previous label; for a subroute that finishes at intermediate vertex $v^i_L$ |
| $I_L = [a_L, b_L]$ | Time period for label $L$ (the earliest and latest times that the truck could reach $v_L$) |
| $V_Q = \{v_1, \ldots, v_{\text{end}}\}$ | The list of vertices that a truck is required to visit                      |
| $Q_i = (v_{\text{start}}, V_Q, \tau_{\text{start}})$ | Request to route truck $t_i$ from $v_{\text{start}} \in V$ to each vertex in $V_Q$ in turn, starting at time $\tau_{\text{start}}$ |
| $\tau_{\text{in}}$ and $\tau_{\text{out}}$ | In and out times for an edge                                               |
| $R_i$           | Route constructed for truck $i$                                            |
| $v^i_L$         | Intermediate node that label $L^i$ forms part of the path towards          |
| $\mathcal{L}$  | The set of all of the labels at vertex $v \in V$                           |

The algorithm terminates when a route $R_i$ to the destination vertex is found. The route $R_i$ is reconstructed by following the ancestor $\text{pred}_L$ of each label in turn. $R_i$ is allocated to truck $t_i$, and the $\mathcal{F}(e)$ are trimmed, split or deleted to reflect times that $t_i$ is present on each $e$. If a complete path exists between $v_{\text{start}}$ and $v_{\text{end}}$ on $G$, QPPTW will always return a route: delay caused by conflicts with other vehicles will simply make the time of arrival at the target vertex $v_{\text{end}}$ later. The time complexity of QPPTW is polynomial in the number of time-windows: $O(|\mathcal{F}|^3 \log |\mathcal{F}|)$ [18].
Algorithm 1 QPPTW: additional steps for QPPTW-m in blue (color figure online)

Input: Graph $G = (V, E)$ with weights $\tau_e$ for all $e \in E$, the set of sorted time-windows $\mathcal{F}(e)$ for all $e \in E$, a routing request $Q_i = (v_{start}, V_Q, t_{start})$ with the source vertex $v_{start} \in V$, the list of vertices to visit in-order $V_Q = \{v_1, \ldots, v_{end}\} \in V$ and the start time $t_{start}$.

Output: Quickest conflict-free route $R$ from $v_{start}$ to $v_{end}$ via each vertex in $V_Q$, starting at the earliest at $t_{start}$, respecting the given time-windows $\mathcal{F}$.

1: Let $H = \emptyset$; Let $\mathcal{L}(v) = \emptyset \forall v \in V$
2: Create new label $L$ such that $L = (v_{start}, [t_1, \infty), nil, v_1)$
3: Insert $L$ into heap $H$ with key $\tau_1$; Insert $L$ into set $\mathcal{L}(v_{start})$
4: while $H \neq \emptyset$ do
5: Let $L = H.getMin()$, where $L = (v_L, I_L, pred_L, v_L^\prime)$ and $I_L = [a_L, b_L]$
6: if $v_L = v_L^\prime$ then \Comment{Label represents route to intermediate target}
7: if $v_L = v_{end}$ then \Comment{Actually, a route to the final target}
8: from $L$, rebuild route $R$ from $v_{start}$ to $v_{end}$ and return $R$
9: else \Comment{A route to an intermediate vertex}
10: $v_L^\prime = v_L^\prime + 1$
11: $a_{load} = a_L + \tau_{v_L}$ \Comment{Update sub-route end to next intermediate point}
12: $L_{load} = (v_L, (t_1, \infty), L, v_L^\prime)$ \Comment{Earliest end time for loading period}
13: $L = L_{load}$ \Comment{Add label for loading period}
14: end if
15: end if
16: for all outgoing edges $e_L$ of $v_L$ do
17: for each $F_{e_L}^j \in \text{tailset}(\mathcal{F}(e_L), a_L)$, where $F_{e_L}^j = [a_{e_L}^j, b_{e_L}^j]$ do \Comment{Expand labels for edges where time intervals overlap:}
18: if $a_{e_L}^j > b_L$ then \Comment{Consider next outgoing edge (Line 16)}
19: next $e_L$
20: end if
21: if $b_{e_L}^j < a_L$ then \Comment{Consider next time-window (Line 17)}
22: next $F_{e_L}^j$
23: end if
24: Let $\tau_{in} = \max(a_L, a_{e_L}^j)$, $\tau_{out} = \tau_{in} + \tau_{e_L}$
25: if isLoading($v_L$) then
26: Let $\tau_{out\_check} = \tau_{out} + \tau_{v_L}$
27: end if
28: else
29: Let $\tau_{out\_check} = \tau_{out}$
30: end if
31: if $\tau_{out\_check} \leq b_{e_L}^j$ then \Comment{Dominance check}
32: Let $u = \text{head}(e_L)$
33: Let $L' = (u, [\tau_{out}, b_{e_L}^j], L)$
34: for each $\hat{L} \in \mathcal{L}(u)$ do \Comment{only check labels for same subroute}
35: if $v_L^\prime = v_L^\prime$ then \Comment{Next time-window (Line 17)}
36: if $\hat{L}$ dominates $L'$ then \Comment{Next time-window (Line 17)}
37: next $F_{e_L}^j$
38: end if
39: if $L'$ dominates $\hat{L}$ then
40: Remove $\hat{L}$ from $H$ and from $\mathcal{L}(u)$
41: end if
42: end if
43: end for
44: end if
45: end if
46: end for
47: end while
48: return “no $v_{start}$ to $v_{end}$ route exists”
4.2 Additions to QPPTW

Our proposed extension is simple: the addition of a stack containing the intermediate vertices to visit. The head of the stack is used as the target vertex, and when reached, is removed so the algorithm can continue the route towards the next target. We also add “wait” periods, which extend the time periods for labels on intermediate vertices to accommodate the truck loading operation. The precise changes to the algorithm are summarised below, and highlighted in Algorithm 1. We term the extended algorithm QPPTW-m (QPPTW for multiple points).

1. The definition of labels is extended to include a reference to the intermediate node $v_i$ that the label forms part of the path towards. The inputs to the algorithm are amended: rather than only a destination vertex $v_{end}$, a list of vertices to visit in-order $V_Q$ is provided. Consequently, Step 2 is amended so the first label $L$ is created with the first vertex to visit in $V$.

2. At Step 9 a new if statement is added. The original QPPTW checks here whether the current label represents a route to the target, and if so, returns the route (Steps 7–8). We add a check to determine whether the present label represents a route to the intermediate target $v_i$. If $v_i$ is also the final target, we return the complete route as before. If not, we update the intermediate target to the next vertex in $V_Q$ (Steps 10–13).

3. Each intermediate vertex involves a loading operation, so we update the earliest time the truck can leave $v_i$ by adding the loading time (Step 11). Loading time is determined by the level accessed. We then create a new label $L_{load}$ for $v_i$ for the new times (Step 12).

4. There is no need to add the new label to the heap as it will just be removed at the next stage. Rather, the label that was obtained from the heap ($L$) is replaced with the newly created one ($L_{load}$) (Step 13). $L_{load}$ will be used as the parent for any further expansion of the route.

5. At Steps 26–29, a new variable $\tau_{out\_check}$ is created. $\tau_{out}$ is the estimated exit time for the edge currently considered to expand the route. $\tau_{out\_check}$ includes loading time if the vertex reached by the edge has a loading operation. $\tau_{out\_check}$ is then used to check against the current time-window, so the route will only be expanded if the current edge has a time-window long enough to accommodate both loading and edge traversal. Time-windows are also updated to reflect conflicting edges so this ensures no conflicts with other trucks while the present route’s truck is loading.

6. At Step 35, an extra if, so the new label $v'$ is only checked for dominance against labels for the same sub-route (i.e. the same intermediate target $v_i$).

7. We also propose a change to improve efficiency at Step 17. The available time-windows $\mathcal{F}(e_L)$ for each edge $e_L$ are stored in a sorted set, in order of ascending end time. Rather than iterating over the whole set $\mathcal{F}(e_L)$, the tail set is used, starting with the first window to end after the current label’s start time. This way, we only consider time-windows that can be used by the truck.
4.3 Higher level search

Outside the core algorithm, there are two levels to the problem to consider. Clearly, the order in which the intermediate points are visited has an impact on collection time. This can be formulated as a search over permutations, the well-known Travelling Salesman Problem, an instance of which exists for each collection trip. Furthermore, the order in which routes are allocated to vehicles has been shown to make a small, but nevertheless notable, difference to total transit times for QPPTW \[4,17\]. Simply, because the routes are reserved via the time-windows, it is possible for an earlier truck to be routed in such a way that it prevents several later trucks being routed optimally. Merely allocating the routes in a different order, without changing their start times, can avert this problem. So, we have a permutation of length \(n\) trips for which routes need allocated, and \(n\) permutations of varying lengths (one per trip).

5 In practice

We ask two questions: (Q1) Does the approach solve the problem? (Q2) Is the approach suitable for real-world use? Q1 can easily be answered. For the real-world scenario described in Sect. 3.1, with 57 truck movements (covering around 6 h), the algorithm was able to allocate conflict-free routes. Precise comparisons with the existing manual-routing approach cannot be made because the existing routes were not recorded. However, PostPac was satisfied that the automated routes were superior to manual allocation.

For Q2, a single run of QPPTW-m allocated routes within 5 s, in Java running on a standard Intel™ i7 CPU. We noted above that the approach is impacted by the order of both intermediate vertices and the order in which routes are allocated; consequently for real-time use we should consider the total run time of the high-level metaheuristic search over these permutations. To explore this, simple experimental runs were carried out with a hillclimber (HC) and simulated annealing (SA), implemented with the Haiku toolkit \[10\].

The representation was a set of permutations: one for the trips to route, and, for each trip, a permutation of items to collect (i.e. locations to visit). Both metaheuristics used two perturbation operators, chosen with equal probability: (1) swap trips to route; and (2) swap items for collection within a trip chosen at random. The objective to minimise was total collection time, as computed for the routes returned by QPPTW-m, assuming an average speed of 1 unit of storage space per second and loading times of 30, 180 and 300 s for items on levels 1, 2, and 3 respectively. The specific instance allocated routes for 10 trucks; more importantly these needed routes allocated for 57 trips in total. Both algorithms were run for 1000 evaluations. Item locations and requirements for each order were allocated at random, with allocations of items to specific truck trips determined by an earlier optimisation run. The problem scenario and results are available at the URL given at the end of the paper.

Table 2 shows results from both algorithms, aggregated over 30 independent runs. Also given as a reference are the results for 1000 randomly generated permutations. The results were not normally distributed, so medians and interquartile ranges are given.
Table 2: Total time (s) for the routes allocated by QPPTW-m, and run times (s): for a single run of QPPTW-m using a randomly generated permutation of items and trucks; and for a run of a hillclimber and simulated annealing over 1000 evaluations each

| Algorithm                  | Total route duration | Run time    |
|----------------------------|----------------------|-------------|
| Random (single)            | 258409\textsubscript{4985} | 4.480\textsubscript{43} |
| Hillclimber (1000 evals)   | 245955\textsubscript{1533} | 3621\textsubscript{329} |
| Simulated annealing (1000 evals) | 246135\textsubscript{1412} | 3734\textsubscript{280} |

Values are medians over 1000 runs (random) and 30 runs (HC/SA), with interquartile ranges in subscript.

Table 3: Total time (s) for the routes allocated by Dijkstra’s algorithm, and run times (s)

| Algorithm                  | Total route duration | Run time    | Conflicts  |
|----------------------------|----------------------|-------------|------------|
| Random (single)            | 63752\textsubscript{276} | 0.204\textsubscript{008} | 875\textsubscript{345} |
| Hillclimber (1000 evals)   | 62798\textsubscript{234} | 1962\textsubscript{45} | 881.5\textsubscript{238} |
| Simulated annealing (1000 evals) | 62781\textsubscript{196} | 1972\textsubscript{94} | 875.5\textsubscript{241} |

As with Table 2, results for random permutations, and a run of a hillclimber and simulated annealing over 1000 evaluations each. The final column shows the number of conflicts introduced by these route allocations. Values are medians over 1000 runs (random) and 30 runs (HC/SA), with interquartile ranges in subscript.

HC found the shortest route times for our specific scenarios, though the difference with SA was found to not be statistically significant. Both HC and SA showed a significant improvement over random permutations, of around 5% total route time. A single run of QPPTW-m for the several hours’ worth of truck movements using a randomly generated permutation takes 4–5 s. The run times for both metaheuristics are around an hour and so are indeed practical for real-world use, if planning schedules ahead of time.

This was compared to a baseline approach of running Dijkstra’s shortest path algorithm [7] to allocate the routes to each truck in turn. The results for this, using the same approaches for determining the permutations of trips to route and items to collect, are given in Table 3. It is clear that this approach finds shorter paths overall, in a much shorter time. However, as this approach did not consider conflicts, we checked how many occasions these routes would result in multiple trucks sharing an edge (a conflict). This is shown in the final column of Table 3. Conflicts occurred over 800 times during the 51 movements. The large number of conflicts to be avoided provides some explanation for the much longer route durations using QPPTW-m.

5.1 Impact of tail set

We tested the impact of changing the original QPPTW algorithm to iterate only over tail sets (Algorithm 1, Step 17). Repeating the experiment above, we generated 1000 random instances of the routing problem (that is, random permutations of trips to route and items to collect). Two variants of QPPTW-m were run for each instance: one using the tail set, and one iterating over the full set of time-windows. The count of iterations of the inner loop was then recorded. The histogram of both counts over the 1000 runs was determined to be normally-distributed. Without the use of a tail set,
the loop ran a mean of 134,660,652 times; with the tail set it ran a mean of 3,584,477 times. A two-tailed $t$-test on these two distributions found $p < 0.001$, suggesting that the addition of tail set leads to a significant reduction in iterations of the QPPTW inner loop.

6 Conclusions

We have presented an extension of the original QPPTW conflict-free routing algorithm from [9] for routes with multiple stops. This is accompanied by a top-level metaheuristic to choose the order in which stops should be visited and the order in which to allocate routes to the vehicles. The approach was demonstrated to run in a reasonable time for a real-world application.

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Data access statement The source code of the proposed algorithm, the scenario used in the experiment and generated results can be obtained from http://hdl.handle.net/11667/130.

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