Finite temperature behavior of impurity doped Lithium cluster

viz Li₆Sn.

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Abstract

We have carried out extensive isokinetic ab initio molecular dynamic simulations to investigate the finite temperature properties of the impurity doped cluster Li₆Sn along with the host cluster Li₇. The data obtained from about 20 temperatures and total simulation time of at least 3 ns is used to extract thermodynamical quantities like canonical specific heat. We observe a substantial charge transfer from all Li atoms to Sn which in turn weakens the Li-Li bonds in Li₆Sn compared to the bonds in Li₇. This weakening of bonds changes the finite temperature behavior of Li₆Sn significantly. Firstly, Li₆Sn becomes liquid-like around 250 K, a much lower temperature than that of Li₇ (≈ 425 K). Secondly, an additional quasirotational motion of lithium atoms appears at lower temperatures giving rise to a shoulder around 50 K in the specific heat curve of Li₆Sn. The peak in the specific heat of Li₇ is very broad and the specific heat does not show any premelting features.
I. INTRODUCTION

Small clusters are known to behave differently than their bulk counterparts, mainly because of their finite size. The finite size effects are reflected in the most of their properties, like equilibrium geometries, energetics, optical properties, ionization potential, polarizabilities, etc.\(^1,2,3,4,5\) For example, equilibrium geometries of small as well as medium size clusters are considerably different than the bulk structures. Stability of a class of clusters depends on the filling up of geometric or electronic shell. The well known example of such a stability is that of alkali metal clusters displaying magic numbers. Further, the properties of homogeneous clusters may be altered, some times quite significantly by adding an impurity. In the last few years some work has been reported on the impurity doped clusters\(^6,7\). These studies have brought out a number of interesting aspects like trapping of an impurity, modifications in the equilibrium structures, changes in the bonding characteristics and enhancement or otherwise in the stability. A few studies have also been reported on the optical properties. Many of these properties have been shown to get influenced by the relative difference in the valence, ionic radii and electronegativity.

A majority of the investigations on heterogeneous and homogeneous clusters pertain to the ground state properties. During the last few years a number of experimental\(^8,9\) and theoretical\(^10,11,12\) studies on finite temperature behavior of clusters have been reported. Finite temperature behavior of homogeneous clusters turns out to be very intriguing and has brought out many interesting features in contrast to the bulk behavior\(^13\). For instance, clusters exhibit a broad peak in the specific heat which is sometimes accompanied by a premelting feature like a shoulder indicating possible isomerization. Recent experiments\(^9\) and simulations\(^11,12\) on tin clusters have shown that these clusters become liquidlike at higher temperatures than the bulk melting temperature (\(T_{m_{\text{bulk}}}\)) contrary to the belief that solidlike to liquidlike transition in the finite size systems occurs at a temperature lower than \(T_{m_{\text{bulk}}}\) because of the surface effects. A number of experiments on Na clusters by Haberland and co-workers\(^8\) have demonstrated that there is no systematic size dependence observed in the melting temperature of clusters between sizes 50 to 200. More interestingly, the peaks in the melting temperature as function of size do not occur at the geometric or electronic shell closing.

In the present work, we investigate the finite temperature behavior of Li\(_6\)Sn and Li\(_7\).
Since the impurity is known to change the geometry as well as bonding substantially in the host cluster it is also expected to change the finite temperature properties of the host cluster. The motivation for investigating these clusters comes from our previous study of Sn doped Li clusters\(^{14}\). This study has shown that, doping of lithium cluster with a tetravalent impurity such as Sn, induces a charge transfer from Li to Sn and as a result the nature of bonding changes from metallic like to dominantly ionic like. Preliminary investigation of the finite temperature behavior of Li\(_6\)Sn has also indicated that this charge transfer induces dramatic effects at low temperatures. The interest in these systems also stems from the anomalous behavior seen in the bulk properties (e.g. electrical resistivity, density, stability function) of Li-Group IV alloys as a function of composition\(^{15}\). These alloys show peak in the resistivity around 20% Sn composition and this has been interpreted as atomic clustering around Sn at this composition whereas other alkali metal-Group IV alloys show peak in the resistivity around 50% composition of Group IV elements. It has also been observed that Li-Si alloys\(^ {16}\) show 15% volume contraction in the liquid state for Si concentration between 15% to 50% whereas in Na-Sn alloys\(^ {17}\) melting takes place via rotor phase in which alkali atoms are supposed to diffuse freely while the group IV polyanions perform only rotational or vibrational movement.

As we shall demonstrate in this paper, the impurity induces a quasirotational motion of alkali atoms around Sn at low temperatures. In addition, in the liquid-like state the value of root mean square bond length fluctuations (\(\delta_{\text{rms}}\)) of impurity doped cluster turns out to be considerably lower than that of Li\(_7\) indicating that volume expansion upon melting is much less in this cluster. Although it is difficult to establish a direct correlation between the properties of the bulk alloys and a small cluster like Li\(_6\)Sn, we believe that the physics of impurity induced effects in both the systems essentially has the same origin arising out of the charge transfer which results into the strong ionic bond.

It is now well established that for reliable ion dynamics one must reproduce the bonding properly. Description of ion dynamics critically depends on the correct microscopic description of instantaneous state of electrons as system evolves in time. This is especially true when the nature of bonding may change during evolution of the trajectories at different temperatures. Therefore, for obtaining reliable ion dynamics we have chosen to use density functional theory (DFT). Small size of the system has permitted us to perform \textit{ab initio} calculations for substantially larger simulation time as compared to the previously published
The paper is organized as follows. In Sec. II we describe briefly our computational and statistical approaches. Results for the equilibrium geometries, nature of bonding and finite temperature properties are given in Sec. III and the conclusions are given in Sec. IV.

II. COMPUTATIONAL DETAILS

All the calculations have been performed using the Kohn-Sham formulation of density-functional molecular dynamics (MD), using the nonlocal norm-conserving pseudopotentials of Bachelet et al. in Kleinman-Bylander form with the Ceperley-Alder exchange-correlation functional. A cubic supercell of length 30 a.u. is used with energy cutoff of 15 Ry. for Li$_6$Sn and 12 Ry. for Li$_7$, which is found to provide sufficient convergence in total electronic energy($E_{tot}$). To have a sufficiently precise evaluation of the Hellmann-Feynman forces on the ions, we ensure that the residual norm of each KS orbital, defined as $|H_{KS}\psi_i - \epsilon_i\psi_i|^2$ ($\epsilon_i$ being the eigenvalue corresponding to eigenstate $\psi_i$ of the KS Hamiltonian $H_{KS}$), was maintained at $10^{-12}$ a.u. After every ionic movement the total electronic energy is converged up to $10^{-5}$ a.u. for low temperatures ($T \leq 200$ K) and the convergence is $10^{-4}$ a.u. for higher temperatures. Such a high convergence is not warranted in the simulated annealing runs but it is very crucial for probing finite temperature behavior of impurity doped clusters. The ground state and other equilibrium structures have been found by carrying out several steepest-descent runs starting from structures chosen periodically from a high-temperature simulation.

The ionic phase space is sampled by isokinetic MD in which the kinetic energy is held constant using velocity scaling. For Li$_7$ we split the temperature range 100 K $\leq T \leq$ 1000 K into about 20 different temperatures, performing up to 90 ps of simulation for lower temperatures (i.e. $T \leq 200$) and 150-200 ps for higher temperatures. For Li$_6$Sn we split the temperature range 10 K $\leq T \leq$ 900 K into about 23 different temperatures, performing up to 200 ps of simulation for lower temperatures (i.e. $T \leq 200$) and 150 ps for higher temperatures. This results into total simulation time about 3 ns for Li$_7$ and 5 ns for Li$_6$Sn.

The data obtained from these extensive simulations is used to extract different thermodynamic quantities such as entropy, specific heat, etc. The ionic specific heat is calculated...
FIG. 1: Comparison of PED for 40 K and 175 K using different criteria for convergence in the total electronic energy ($\Delta E_{\text{SCF}}$). (a) denotes $\Delta E_{\text{SCF}} = 0.00001$ a.u. and (b) denotes $\Delta E_{\text{SCF}} = 0.0001$ a.u.

from the fluctuations in the internal energy of the system and is given by,

$$C(T) = \frac{3Nk_B}{2} + \frac{1}{k_B T^2} (\langle V^2 \rangle_t - \langle V \rangle_t^2),$$

where $V$ is total electronic energy and $\langle \cdots \rangle_t$ denotes time averaged over the entire trajectory. A smooth specific heat can be obtained by using multiple histogram (MH) technique. With multi histogram fit, which is basically a least square fit we extract density of states ($\Omega(E)$) or entropy ($S(E) = k_B \ln \Omega(E)$). From entropy we can compute various thermodynamic quantities like canonical specific heat, $C(T) = \partial U(T)/\partial T$, where $U(T) = \int E p(E,T) dE$ is the average total energy, and where the probability of observing an energy $E$ at a temperature $T$ is given by the Gibbs distribution $p(E,T) = \Omega(E) \exp(-E/k_B T)/Z(T)$, with $Z(T)$ the normalizing canonical partition function.

Along with these thermodynamic quantities we also analyze the data using tradition parameters such as the $\delta_{\text{rms}}$, defined as

$$\delta_{\text{rms}} = \frac{2}{N(N-1)} \sum_{I> J} \frac{(\langle R_{IJ}^2 \rangle_t - \langle R_{IJ}\rangle_t^2)^{1/2}}{\langle R_{IJ} \rangle_t},$$

where $N$ is the number of ions in the system, $R_{IJ}$ is the distance between ions $I$ and $J$, and $\langle \cdots \rangle_t$ denotes a time average over the entire trajectory.
We would like to make few pertinent comments on some technical issues which are specific to \textit{ab initio} simulations. Since such DFT simulations are quite expensive, a judicious choice of simulation time step ($\Delta t$), criteria for the convergence in the total electronic energy during Born-Oppenheimer MD ($\Delta E_{\text{SCF}}$) and total simulation time has to be made. Some of these issues may not be very crucial for geometry optimization, since there the details of ion dynamics are secondary. However for reliable extraction of thermodynamic data, the ion dynamics should be faithfully simulated using the accurate forces. Since the calculation of forces involves the total electronic energy ($E_{\text{tot}}$), the choice of $\Delta E_{\text{SCF}}$ can turn out to be crucial. We demonstrate this point by showing potential energy distribution (PED) (shown in Fig. 1) calculated using two different $\Delta E_{\text{SCF}}$ criteria, 0.0001 and 0.00001 a.u., for two temperatures 40 K and 175 K. Let us recall that PED(E,T) denotes accessible energy states between $E$ and $E + dE$ (where $E$ is total electronic energy of the system). Fig. 1 clearly shows that two different $\Delta E_{\text{SCF}}$ leads to considerably different PEDs. The height of the peak in curve (a) (i.e. $\Delta E_{\text{SCF}} = 0.00001$ a.u.) is about 25% higher than the curve (b) (i.e. $\Delta E_{\text{SCF}} = 0.0001$ a.u.) at 40 K. Further, it can be seen that the lower accuracy curve is seen to span a broader energy range and we have verified that this leads to the erroneous specific heat in this range of temperatures. However as the temperature rises lower criteria can be used without loss of accuracy.

III. RESULTS AND DISCUSSIONS

A. Finite temperature behavior of host cluster: Li$_7$

We begin our discussion by examining the equilibrium geometries of Li$_7$ (shown in Fig. 2). The ground state structure is a pentagonal bipyramid with D$_{5h}$ symmetry. The excited state is tricapped tetragon (C$_{2v}$ symmetry) with 0.22 eV higher in energy compared to the ground state. These geometries are consistent with the earlier reported work. As expected the charge distribution is completely delocalized indicating metallic like bonding in this cluster (not shown).

Before discussing the thermodynamic quantities like specific heat it is instructive to examine normalized potential energy distribution (PED) obtained via our molecular dynamic simulations, as a function of temperature. In Fig. 3 we show PED for different temperatures.
FIG. 2: The ground state and the first excited state geometry of Li$_7$. $\Delta E$ represents difference in the total energies.

FIG. 3: Normalized potential energy distribution of Li$_7$ for some relevant temperatures; viz 150 K, 200 K, 240 K, 280 K, 320 K, 400 K and 500 K. It should be noted that PED for 400 K and 500 K are very flat and almost overlapping ranging from 150 K to 500 K. It may be noted from Fig. 3 that the PED for low temperatures is very sharp and narrow indicating that the system spans a very restricted range of energies. Indeed the observed motion at these temperatures shows that atoms oscillate around their equilibrium positions. As temperature increases the pumped in energy is used to break some of the bonds and as a result cluster spans wider configuration space which reflects in the
FIG. 4: The canonical ionic specific heat of Li$_7$. (a): Computed directly from fluctuations using Eq. 1 with 75 ps for temperatures up to 200 K and 150 ps or more for higher temperatures. (b): The specific heat curve calculated using multihisto fit.

broader PED. We note that around 400 K the PED becomes very flat which indicates that the cluster is spanning large number of energy states with equal probability. This rather broad PED around 400 K and above as compared to the PED for lower temperatures is suggestive of liquid-like nature of the cluster in this range of temperatures.

Some insight can be gained by observing the detailed motion (the movie) of the cluster at few interesting temperature. We note that, around 360 K cluster starts revisiting the ground state via the first excited state and during this process, atoms from the pentagonal ring and atoms capping the ring get interchanged. This processes of interchanging of atoms,
FIG. 5: Root mean square bond length fluctuations of Li$_7$ and Li$_6$Sn. The slow monotonous rise in $\delta_{\text{rms}}$ for Li$_7$ below 320 K indicates solid-like behavior whereas linear nature above 450 K shows liquid-like behavior. For Li$_6$Sn the Lindmann criteria gets satisfied at much lower temperature (around 175 K). We also note that for Li$_6$Sn the value of $\delta_{\text{rms}}$ remains considerably constant for a wide range of temperature i.e. from 250 K to 700 K.

becomes more frequent with increasing temperature. Indeed as we shall see this behavior leads to the peak in the specific heat around 425 K. In Fig. 4 we show ionic specific heat of Li$_7$ calculated using Eq. 1 directly (shown in Fig. 4a) as well as with the multiple histogram technique (shown in Fig. 4b). Evidently, both the methods yield similar specific heat except that specific heat by MH is much smoother. We note that the specific heat is very broad and does not change significantly after the peak around 425 K. Such a broad peak in the specific heat is a characteristic of small clusters in contrast to the sharp transition observed in the extended systems.

These observations are also supported by the $\delta_{\text{rms}}$ which is shown in Fig. 5. As the name suggest $\delta_{\text{rms}}$ indicates fluctuations in the bond lengths averaged over all pairs and simulation time. According to the Lindmann criteria the clusters are considered to be in the liquid-like state when $\delta_{\text{rms}}$ exceeds 0.1. It is interesting to note that $\delta_{\text{rms}}$ shows three distinct regions, a solid-like region below 320 K and a liquid-like region above 450 K. 320 K to 450 K is a
transition region and the value of $\delta_{\text{rms}}$ rises sharply in this region. If we chose to use the Lindmann criteria to estimate the “melting temperature” then this cluster “melts” between 320 K to 360 K.

To summarize, the specific heat curve indicates that above 425 K Li$_7$ is definitely liquid-like and the transition is characterized by rather broad peak in the specific heat. These features are consistent with the specific heat of Li$_8$ reported in Ref. [25]. Both these clusters namely Li$_7$ and Li$_8$ do not show any premelting features.

B. Finite temperature behavior of impurity doped cluster: Li$_6$Sn

In this section we present our results on the impurity doped cluster, namely Li$_6$Sn and contrast the behavior with that of host cluster Li$_7$.

Before studying these finite temperature effects let us examine the equilibrium structures of Li$_6$Sn which are shown in Fig. 6. Firstly, we note that both the geometries are considerably different than that of Li$_7$. Secondly, in the ground state, Sn has six fold coordination whereas the first excited state which is 0.16 eV above the ground state, has five fold coordination with Li atoms. Thus the first excited state has one less Li-Sn bond. Further, these two structures can be obtained by capping the most stable Li$_4$Sn tetrahedron in two different ways.

Now we turn to the bonding features of the system. Our earlier work has shown that a tetravalent impurity like Sn in lithium clusters changes the delocalized metallic like bonding to dominantly ionic like. In Fig. 7 we show the difference charge density of Li$_6$Sn, defined as

\[ \Delta E = 0.0 \text{ eV} \quad \Delta E = 0.16 \text{ eV} \]
FIG. 7: The isosurfaces for difference charge-density of Li₆Sn. (a): charge gained region, (b): charge depletion region. Sn is shown by the black sphere at the center whereas white spheres indicate Li atoms.

FIG. 8: Quasirotational motion of Li atoms around Sn; (a): the ground state geometry (b and c): two Li-Li bonds are broken and the Li atoms get separated into two bunches which form a quasirotational motion around Sn. (d): The resultant geometry. We note that (a) and (d) denotes same geometries with different orientation.

the difference between the selfconsistent charge density and the superimposed atomic charge density. Quite clearly, the charge gained region is mainly around Sn whereas the charge depletion region is near all Li atoms. This clearly shows that there is a charge transfer from all Li atoms to Sn, filling in the Sn centered $p$ orbitals$^{26}$. Typically the depleted charge is of the order of $2/3$ electron per Li atom. As a consequence of the significant charge transfer from Li to Sn, considerable depletion of charge in the region of Li-Li bond is observed which results into weakening of Li-Li bond. This weakening of Li-Li bonds show dramatic effects on the finite temperature behavior of the cluster.

The consequences of weakening of Li-Li bonds are observed at very low temperatures. Around 30 K two Li-Li bonds break and Li atoms get separated into two bunches (see Fig. 8).
FIG. 9: Normalized Potential Energy Distribution at 150 K and 400 K of Li$_6$Sn and Li$_7$.

These bunches perform a quasirotational motion around Sn as shown in Fig. 8. We note from Fig. 8 that the initial (Fig. 8a) and final (Fig. 8d) geometries are same but have different orientations. Since the motion is observed at very low temperatures the potential barrier joining these two (identical) structures must be very low. This quasirotational motion seen at such a low temperature shows up in the PED of Li$_6$Sn. In Fig. 9 we compare PED of Li$_6$Sn with that of Li$_7$. Evidently, at 150 K the PED of Li$_6$Sn is significantly different than that of Li$_7$. A rather narrow and sharp distribution for Li$_7$ indicates that it is showing clear solid-like behavior exhibiting small oscillations at this temperature, whereas the significantly broader distribution of Li$_6$Sn shows that other modes of excitations are also available to the system at this temperature. In fact the observed motion at this temperature shows breaking of most of the Li-Li bonds. On the other hand at 400 K the PED of both clusters have similar shapes.

Turning to the ionic specific heat of Li$_6$Sn (shown in Fig. 10) we note that the specific heat curve is significantly different than that of Li$_7$. Unlike Li$_7$, it shows a shoulder around 50 K and the main peak is observed at substantially lower temperature (i.e. 250 K) compared to that of Li$_7$ (425 K). The shoulder in the specific heat curve of Li$_6$Sn corresponds to the quasirotational motion described earlier. As temperature rises further this quasirotational motion becomes more rigorous and eventually around 200 K the bunches of Li atoms lose their identity and exhibit diffusive motion around Sn. This leads to the peak around 250 K.
FIG. 10: The canonical ionic specific heat of Li$_6$Sn. The shoulder around 50 K is because of the quasirotational motion seen at that temperature whereas the peak is around 250 K, a substantially low temperature compared to that of Li$_7$.

These observations are also consistent with the $\delta_{\text{rms}}$ which is shown in Fig. 5 along with the $\delta_{\text{rms}}$ for Li$_7$. For Li$_6$Sn the value of $\delta_{\text{rms}}$ rises in two distinct steps. The first step is around 30 K. We recall that quasirotational motion starts around this temperature and another step is around 200 K where the bunches of Li atoms lose their identity and diffuse around Sn.

It is also observed that the value of $\delta_{\text{rms}}$ remains nearly constant between 250 to 700 K. Although this effect is small it is noteworthy. In this temperature range the system is liquid-like but instead of random diffusive motion of all atoms in the cluster we observe that Li atoms perform constrained diffusive motion with Sn at the center. The averaged fluctuations in Li-Sn bond in this range of temperatures is found to be within 15%. These observations indicate that the main peak around 250 K is associated with the breaking of weak Li-Li bonds. We also note that in Li$_6$Sn though $\delta_{\text{rms}}$ satisfies the Lindmann criteria at very low temperature compared to that of Li$_7$, its saturated value is 0.17 which is considerably lower compared to the host Li$_7$ ($\delta_{\text{rms}} = 0.25$) cluster. This indicates that in the liquid state the volume expansion of the impurity system is much less than in the case of host cluster. This is consistent with the existence of stronger Li-Sn bond in the system. At still higher
temperatures one of the ionic bonds breaks and we observe the first excited state (shown in Fig. 6) in which Sn has one less coordination number than the ground state. Thus the route for evaporation proceeds via the first excited state.

Finally we note that, Li$_6$Sn is an over lithiated cluster, i.e. the number of Li atoms in the cluster are more than those required to complete the $p$ shell of Sn atom. It will be interesting to investigate the finite temperature behavior of a cluster which satisfy the octate rule i.e. like Li$_{4x}$Sn$_x$. In these clusters though we expect that because of complete charge transfer from all Li atoms to Sn, the bonds between Li atoms will be extremely weak, the ionic bond between Li-Sn will be more strong than those in the overlithiated cluster like Li$_6$Sn.

IV. CONCLUSIONS

We have presented an ab initio isokinetic MD simulations on Li$_6$Sn and Li$_7$ to demonstrate the dramatic effects induced by the impurity in the host cluster. The key point which emerges out of these calculations is that the essential physics governing these effects comes from the charge transfer from Li to Sn because of the large difference in their electronegativities. In Li$_6$Sn, we observe a quasirotational motion at very low temperature which gives rise to a shoulder in the specific heat curve around 50 K. The main peak is observed at much lower temperature, around 250 K, compared to the host cluster ($\approx$ 425 K) whereas Li$_7$ shows a broad peak in the specific heat with no premelting features. The motion in the liquid state of Li$_6$Sn is essentially a constrained motion of Li atoms around Sn center.

Acknowledgments

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26 We have examined the relevant occupied orbitals and have observed that all the orbitals are centered around Sn.

27 We have verified the existence of this small shoulder by carrying out a number of additional simulations between 10 K to 100 K.
