Oscillatory behavior and enhancement of the surface plasmon linewidth in embedded noble metal nanoparticles

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Abstract. We study the Landau damping of the surface plasmon resonance of metallic nanoparticles embedded in different environments of experimental relevance. Important oscillations of the plasmon linewidth as a function of the radius of the nanoparticles are obtained from numerical calculations based on the time dependent local density approximation. These size-oscillations are understood, within a semiclassical approximation, as a consequence of correlations in the spectral density of the nanoparticles. We treat inert matrices, as well as the case with an unoccupied conduction band. In the latter case, the plasmon lifetime is greatly reduced with respect to the inert case, but the non-monotonous size-dependence persists.

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1 Introduction

In recent years, the use of femtosecond laser pulses has made it possible to investigate the time evolution of collective and quasi-particle excitations in metallic nanoparticles. In these experiments, the actual time-resolved evolution of the energy transfer to the environment can be studied [1,2,3]. A determining factor in the relaxation processes is the lifetime of the collective excitations (surface plasmons), which for small cluster sizes (0.5 nm ≲ R ≲ 2 nm), is limited by Landau damping (decay into electron-hole pairs). The lifetime of the surface plasmon resonance is thus, not only a problem of fundamental interest, but also important for possible applications.

In the last decade, the analogy of surface plasmons with nuclear giant resonances has been exploited, in order to obtain a physical understanding, as well as analytical and numerical estimations, of the plasmon lifetime [4,5,6,7,8]. Following these approaches, and using a semiclassical formalism, an oscillatory behavior of the level width was determined for free clusters of small sizes (a number of atoms N between N ≈ 20 and N ≈ 1000). These analytical results have been verified against numerical calculations within the time-dependent local density (TDLDA) for a jellium model [8], and the oscillations in the level width with the size of the nanoparticles were shown to arise from the electron-hole density-density correlations in the angular restricted density of states.

The non-monotonous size-dependence of the plasmon lifetime has been experimentally observed in free alkaline metal nanoparticles [9,10], as well as in embedded noble metal clusters [11]. Further experimental and theoretical work would be needed in order to unambiguously characterize the level width oscillations. While the analytical calculations are most easily done for free alkaline clusters, metallic noble metal clusters embedded in a transparent matrix are more conveniently investigated from the experimental point of view [3]. It is then important to study theoretically the size-dependence of plasmon lifetime for embedded particles. This is the purpose of this work, where we extend the results of Ref. [7] to different kinds of environments.

The problem of the plasmon lifetime in metallic nanoparticles embedded in a matrix, is considerably more difficult, and less understood, than in the case of free clusters. The most obvious effect when the clusters are embedded in a dielectric material, is the change produced by the dielectric constant of the matrix, that moves the position of the plasmon resonance according to the Mie formula [13], and can also affect the width of the plasmon [9,11]. Moreover, when the matrix is not inert, it can react with the atoms in the surface of the nanoparticle. The electronic states on the surface are modified and contribute to the loss of coherence of the collective state. This is the so-called chemical interface damping. In addition, the presence of a conduction band in the matrix at an energy accessible to the electrons, weakens the confinement, and contributes to the width of the surface plasmon in an important way. All these different effects can add up and make the theoretical description of the system quite involved.

The experiments of Charlé et al. [11] studied the influence of the matrix environments on surface plasmon excitations of small silver particles. They found a strong broadening of the surface plasmon resonance when the
particles were embedded in a reactive matrix such as CO, as compared to an inert matrix from a noble gas like Ar. This effect has been attributed to chemical interface damping. Also, a very strong broadening has been observed by Hövel et al. [4] for silver particles embedded in SiO$_2$. In a very interesting and pioneering paper, Persson proposed a model for explaining these experimental observations that took into account the modification of the electronic eigenstates of the metallic nanoparticle by the layer of absorbates on its surface and by a conduction band [13].

In the next section we recall the basic theoretical facts of the calculation of the plasmon lifetime within a semiclassical approximation. We then study the linewidth of embedded clusters from TDLDA calculations for inert matrices. The case of matrices with a conduction band is treated in Sec. 4. The theoretical treatment of the chemical interface damping is out of reach of our theoretical description, but the cases that we will consider are not thought to be considerably influenced by this effect.

2 Theoretical background for free clusters

The Landau damping of the dipole plasmon can be calculated treating the collective excitation as an external perturbation, which can give rise to the creation of electron-hole excitations [12]. Then, Fermi’s golden rule yields the width

\[ \Delta \Gamma = \frac{2\pi}{\hbar} \sum_{p} \sum_{h} \delta(h\omega_{\mathcal{M}} - \epsilon_{p} + \epsilon_{h}) \]  

(1)

where \( |p\rangle \) and \( |h\rangle \) are electron and hole states in the self-consistent field, with their energies given by \( \epsilon_{p} \) and \( \epsilon_{h} \), respectively, \( \delta V \) is the dipole field due to the surface plasmon, and \( \omega_{\mathcal{M}} \) is the frequency of the plasmon, which classically is given by the Mie formula,

\[ \omega_{\mathcal{M}} = \sqrt{\frac{\omega_{p}}{\epsilon_{d} + 2\epsilon_{m}}} \]  

(2)

where \( \omega_{p} \) is the plasma frequency, \( \epsilon_{d} \) is the dielectric function of the \( d \) electrons and \( \epsilon_{m} \) is the dielectric function of the embedding matrix.

In the case of spherical symmetry, assuming that the confinement and the interactions lead to hard walls at radius \( R \) in the self-consistent field, we can evaluate Eq. (1). Integrating over the electron-hole states, one obtains

\[ \Delta \Gamma(R) = c\gamma \int_{E_{F}}^{E_{F} + h\omega_{\mathcal{M}}} dE \sum_{L} \sum_{L' = L - 1} (2L + 1)(2L' + 1) \times \sum_{<L, 0; 0|L', 0>} ^{E_{F} + h\omega_{\mathcal{M}}} E(E - h\omega_{\mathcal{M}})d_{L}(E)d_{L'}(E - h\omega_{\mathcal{M}}), \]  

(3)

where \( <L, 0; 0|L', 0> \) is a Clebsch-Gordan coefficient, \( \gamma = (2\pi\hbar^{3})/(3NM^{2}\omega_{\mathcal{M}}R^{4}) \), \( c = 4MR^{2}/\hbar^{2} \), \( E_{F} \) is the Fermi energy, and \( d_{L}(E) \) is the one-dimensional density of states with total angular momentum \( L \).

Using the semiclassical expression for the density of states of the one-dimensional problem [14], we can decompose \( d_{L}(E) \) in its smooth (zero-length trajectories) and oscillating components (arising from periodic orbits). We then obtain two contributions to the width of the plasmon resonance

\[ \Delta \Gamma = \Delta \Gamma_{0} + \Delta \Gamma_{osc}. \]  

(4)

The smooth term \( \Delta \Gamma_{0} \) arises from the smooth component of \( d_{L} \) and exhibits the well known \( 1/R \) dependence firstly proposed by Kawabata and Kubo [15].

\[ \Delta \Gamma_{0}(R) = \frac{3\hbar v_{F}}{4R} \left( \frac{\pi}{\hbar} \right) g(\xi), \]  

(5)

where \( \xi = h\omega_{\mathcal{M}}/E_{F} \), \( g(\xi) \) is a smoothly decreasing function with \( g(0) = 1 \), and \( v_{F} \) is the Fermi velocity.

The oscillating part \( \Delta \Gamma_{osc} \) arises from the density oscillations as a function of the energy. Within a semiclassical approach, it can be written as

\[ \Delta \Gamma_{osc} \approx \frac{6\sqrt{2\pi\hbar}}{MR^{2}\sqrt{k_{F}R\xi}} \sum_{r=1}^{\infty} \frac{1}{\sqrt{r}} \cos(2rk_{F}R\xi), \]  

(6)

where the sum runs over all repetitions \( r \) of the period of the equivalent one-dimensional motion. The amplitude of these oscillations can be of the order of \( \Delta \Gamma_{0} \) for small clusters.

3 Embedded metallic clusters in inert matrices

We want to address the question of what happens with the oscillations and the typical value of the linewidth of the plasmon when the nanoparticles are embedded in a matrix. In Ref. [7] we presented some calculations for noble metals embedded in inert matrices. The numerical results were obtained using the TDLDA formulation by Bertsch [18] but modifying the residual interaction to include the frequency-dependent dielectric function of the \( d \) electrons \( \epsilon_{d}(\omega) \) and the dielectric constant of the matrix \( \epsilon_{m} \) [19]. In order to maintain the spherical symmetry of our problem we always considered cluster sizes corresponding to magic numbers of atoms.

For inert matrices, the plasmon linewidth is affected only by the modification of the frequency \( \omega_{\mathcal{M}} \) through the parameter \( \xi \) of Eqs. (5) and (6). This is due to the fact that the self-consistent potential, and, therefore, the electron-hole density-density correlation function are practically unchanged by \( \epsilon_{m} \), but the energy position of the plasmon peak follows the Mie formula. Results for the width of the plasmon in the case of Ag nanoparticles embedded in a matrix of Ar are shown in Fig. 1. In the inset we show a typical spectrum of the photo-absorption cross-section for Ag$_{440}$ embedded in Ar. The singularities of the spectrum are smeared out by a non-zero \( \gamma \). This value of \( \gamma \) is subtracted at the end of the calculation and we verify that the fit of \( \Delta \Gamma \) is not sensitive to it, provided that it is larger than a minimum value. \( \Delta \Gamma^{*} \) exhibits pronounced oscillations as a function of the radius. The smooth part of
the Bohr radius \( a_0 = 0.53 \AA \) for silver nanoparticles in an Ar matrix calculated within TDLDA (full circles) together with the experimental results of Ref. [11] (empty squares). The dashed line through the numerical points is a guide-to-the-eye. The dotted line represents, respectively, \( \Gamma_0(R) \) and \( \Delta \Gamma(R) \) according to Eqs. (4), (5) and (6) (with a reduction factor of 3 as discussed in the text). Inset: logarithm of the TDLDA absorption cross section for \( \text{Ag}_{440} \) \( R/a_0 = 2.2 \), showing the pronounced surface plasmon resonance, fitted by a Lorentzian (dotted line). The excited states are indicated by tick marks and their oscillation strengths given by the height of the vertical lines.

Fig. 1. Linewidth as a function of the radius (in units of the Bohr radius \( a_0 = 0.53 \AA \)) for silver nanoparticles in an Ar matrix calculated within TDLDA (full circles) together with the experimental results of Ref. [11] (empty squares). The dotted line through the numerical points is a guide-to-the-eye. The dashed and the solid lines represent, respectively, \( \Gamma_0(R) \) and \( \Delta \Gamma(R) \) according to Eqs. (4), (5) and (6) (with a reduction factor of 3 as discussed in the text). Inset: logarithm of the TDLDA absorption cross section for \( \text{Ag}_{440} \) \( R/a_0 = 2.2 \), showing the pronounced surface plasmon resonance, fitted by a Lorentzian (dotted line). The excited states are indicated by tick marks and their oscillation strengths given by the height of the vertical lines.

**Fig. 2.** Width of the surface plasmon resonance for silver clusters of two different sizes as a function of \( \epsilon_m \). Inset: frequency of the plasmon \( \omega_M \) together with the expression for the Mie formula (solid line) with a small modification of the bulk \( \omega_p \). The oscillations in the width are very different for the two sizes due to the shell filling and the corresponding density correlation function. Although the range of \( \epsilon_m \) over which we can see the complete oscillation of the plasmon lifetime is very large, it should be possible to observe maxima and minima in experiments, if we are able to change the dielectric constant of the surrounding medium. In the inset of this figure we show the position of the plasmon peak as a function of the \( \epsilon_m \) for the corresponding sizes. The behavior with \( \epsilon_m \) is very well described by the Mie formula, and the two sizes behave in the same way. We can see almost no difference in the position of the plasmon peak between the sizes for the same value of \( \epsilon_m \), but there are great changes in its width.

### 4 Ag nanoparticles embedded in a matrix with a conduction band

The \( \text{SiO}_2 \) used in experiments for embedding Ag nanoparticles is an amorphous solid with a conduction band with a minimum situated at \(-1.7\) eV with respect to the vacuum energy. The valence band maximum occurs \(10.6\) eV below the vacuum energy and has no influence in the Ag-surface plasmon [13]. Chemical interaction in the surface between Ag and the \( \text{SiO}_2 \) is not expected to occur [14] and chemical interface damping does not influence the width of the plasmon in this case. In order to implement the TDLDA calculations, we simulate the embedded medium by a change of the bulk plasmon [15]. Chemical interaction in the surface between Ag and the \( \text{SiO}_2 \) is not expected to occur [14] and chemical interface damping does not influence the width of the plasmon in this case. In order to implement the TDLDA calculations, we simulate the embedded medium by a change of the bulk plasmon.
that the electrons at $E_F$ are less tight, which translates in a small redshift in the position of the plasmon peak due to the bigger spill-out and into an increase (by a factor of 2) of the width (compare with Fig. 3). This is consistent with the factor of 2 enhancement observed in the experiments of Ref. [13]. Although in these experiments the distribution of sizes has certain unknown variance that can increase the results for the linewidth of the optical absorption experiments, a more refined model including the self-interaction correction to the TDLDA, and a corrected dielectric function for the surface, are probably needed for a more quantitative agreement. However, we can clearly see that the non-monotonous behavior is maintained and is of the same order as for free Ag nanoparticles. Other different kinds of glasses that are used in experiments should produce similar increases in the width of the plasmon if the difference between the energy of the minimum of the conduction band and $E_F$ is not too far from the energy of the plasmon.

5 Conclusions

As other size-dependent phenomena in clusters, the width of the plasmon presents a leading-order (smooth) contribution (that goes like $1/R$), with oscillatory corrections due to shell effects. For the plasmon lifetime these size-dependent corrections are much more important than for the position of the resonance. Going for free to embedded clusters makes this difference still more pronounced.

We have shown in this work that the size-dependent oscillations of the linewidth, in free as well as in embedded clusters, arise from electron-hole density correlations. Such an effect can be explored by varying the dielectric constant of the matrix around the nanoparticle.

We have also considered the width of the plasmon for a simple model of nanoparticles of Ag surrounded by a matrix of amorphous SiO$_2$ with a conduction band. The width is increased in a way that agrees semi-quantitatively with the experiments. The oscillations in the width are still present and could be seen in experiments with a narrow distribution of sizes. An adequate choice of the composition of the matrix should make it possible to increase the lifetime of the surface plasmon by tuning its energy to a value where the electron-hole correlation function is nearly zero, which can be useful in certain applications.

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