micrOMEGAs4.1: two dark matter candidates

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Abstract

micrOMEGAs is a code to compute dark matter observables in generic extensions of the standard model. This version of micrOMEGAs includes a generalization of the Boltzmann equations to take into account the possibility of two dark matter candidates. The modification of the relic density calculation to include interactions between the two DM sectors as well as semi-annihilation is presented. Both DM signals in direct and indirect detection are computed as well. An extension of the standard model with two scalar doublets and a singlet is used as an example.

1 Introduction

Strong evidence for dark matter at the scale of galaxies and galaxy clusters is sustained by recent precise cosmological observations by the PLANCK satellite [1]. However, the simplest WIMP paradigm, e.g. within the framework of SUSY, is challenged by collider data since no evidence for new particles was found in the first LHC run [2, 3]. At the same time several anomalies have been observed in both direct detection [4, 5, 6, 7, 8] and indirect detection experiments [9, 10, 11, 12]. The various signals corresponding to vastly different mass scales cannot be explained by a single dark matter candidate. Moreover some of these anomalies hint at cross sections stronger than the canonical value deduced from cosmological observations. While these anomalies cannot be unambiguously associated with dark matter, for example pulsars could be the source of the higher than expected positron flux at high energies [13], and anomalies in direct detection corresponding to light dark matter are challenged by competing experiments with null results [14, 15], these observations raise the interesting possibility that the anomalies could be due to two dark matter candidates.

On the theoretical side, multi-component DM models have been considered a long time ago. For example the idea that the neutrino, the axion or its supersymmetric partner, the axino could constitute a fraction of the total DM has been examined carefully over the years [16, 17, 18, 19]. Models where both components are WIMPs - and could therefore lead to typical signatures at different mass scales - have also been examined [20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34].

When DM is made of two WIMPs the interactions between the two dark matter - so-called dark matter conversion [35, 36], modify the Boltzmann equation and impact the computation of the relic density. Here we generalize the micrOMEGAs routine to compute the relic density to include all possible interactions between the particles in the dark sectors. In particular all semi-annihilation processes (where two dark matter particles annihilate into another dark matter particle and a standard one) are also included. We also add a few facilities to the direct and indirect detection routines to take into account
the contribution of each component to the DM density. As a working example of a multi-component DM model we consider an extension of the SM containing one extra scalar doublet and one scalar singlet. A $Z_4$ discrete symmetry leads to two stable DM candidates and implies both semi-annihilations and self-interactions between the two dark sectors \[24, 34\].

This paper is organized as follows. In section 2 we list all possible DM interactions and mention the $Z_N$ or $Z_N \times Z_M$ discrete groups that could lead to these interactions. The generalization of the relic density calculation and the method used to solve these equations are described in section 3. The modification of the micrOMEGAs routines that deal with two DM candidates are described in section 4. Section 5 contains sample results obtained for the $Z_4$ model with two doublets and a singlet.

### 2 Classification of 2-DM models.

micrOMEGAs exploits the fact that models of dark matter exhibit a discrete symmetry and that the fields of the model transform as

\[ \phi \rightarrow e^{i2\pi X_\phi} \phi \]

where the charge $|X_\phi| < 1$.

The particles of the Standard Model are assumed to transform trivially under the discrete symmetry, $X_\phi = 0$. The lightest particle with charge $X_\phi \neq 0$ will be stable and, if neutral, can be considered as a DM candidate. Typical examples of discrete symmetries used for constructing single DM models are $Z_2$ and $Z_3$. Multi-component DM can arise in models with larger discrete symmetries. A simple example is a model with $Z_2 \times Z_2'$ symmetry, the particles charged under $Z_2(Z_2')$ will belong to the first (second) dark sector. The lightest particle of each sector - whether it is a fermion or a scalar - will be stable and therefore a potential DM candidate. Another example is a model with a $Z_4$ symmetry. The two dark sectors contain particles with $X_\phi = \pm 1/4$ and $X_\phi = 1/2$ respectively. The lightest particle with charge $1/4$ is always stable while the lightest particle of charge $1/2$ is stable only if its decay into two particles of charge $1/4$ is kinematically forbidden.

We can write all possible dimension-4 interactions for models with two dark sectors. Let $\phi_a$ and $\phi_b$ be the generic names of particles belonging to each dark sector, with $X_a \neq \pm X_b \neq 0$. For any choice of discrete group, the potential for scalars can contain the terms

\[ V_0 = m_a^2 \phi_a \bar{\phi}_a + m_b^2 \phi_b \bar{\phi}_b + \lambda_a \phi_a^2 \bar{\phi}_a^2 + \lambda_b \phi_b^2 \bar{\phi}_b^2 + \lambda_{ab} \phi_a \phi_b \bar{\phi}_a \bar{\phi}_b \]

Here we omit isospin indices and assume that $\phi_a(\phi_b)$ represent all the different scalar particles with a given discrete charge. Additional terms are possible depending on the choice of the symmetry group. The list of all possible structures for models with two scalar dark sectors is given in Table 2 together with the lowest $Z_N$ or $Z_N \times Z_M$ symmetry that leads to such interactions. When the dark sector contains fermions and gauge bosons, the number of allowed terms is more limited and can be easily written for each specific case.

\[ ^1 \text{We do not write the generic Lagrangians when the dark sector contains fermions and gauge bosons, this Lagrangian is simpler than for scalars and can be easily adapted for each choice of symmetry and particle content.} \]
\[ n_{\phi} - k_{\phi} X_{\phi} = \frac{3 - \phi_{\phi}}{\n \phi} \]

3.1 Evolution equations

The derivation of the equations for the number density of two DM particles is based on standard assumptions: 1) all particles of the same sector are in thermal equilibrium b) particles of the dark sectors have the same kinetic temperature as those of the SM c) the number densities of DM particles can differ from the equilibrium values when the number density of DM particles times their annihilation cross section becomes too low to

\[ X_a \times X_b \]

Table 1: Table of generic group structures and interaction vertices for 2-component DM models, here \( k, n \) are integers. Hermitian conjugated terms are omitted, the complete list can be obtained swapping \( \phi_a \leftrightarrow \bar{\phi}_a \) and \( \phi_a \leftrightarrow \phi_b \).

The Lagrangian for a concrete multi-component DM model will of course depend on the spin and isospin of the non-standard particles. Consider a model with two scalar doublets \( H_1 \) and \( H_2 \) and a singlet, \( S \). We impose a \( Z_4 \) symmetry with \( X_{H_1} = 0 \), \( X_{H_2} = 1/2 \) and \( X_S = 1/4 \). Both \( H_2 \) and \( S \) are inert, i.e. they do not couple to fermions while \( H_1 \) has couplings similar to those of the SM Higgs, for more details see Ref. [21]. The field \( \phi_a \) stands for the singlet and \( \phi_b \) with the doublet. The potential reads

\[
V_{Z_4} = V_0 + \frac{\lambda_S}{2} (S^2 + S^{14}) + \frac{\lambda_5}{2} \left[ (H_1^1 H_2^1)^2 + (H_2^1 H_1^1)^2 \right] + \frac{\lambda_{S12}}{2} (S^2 H_1^1 H_2^1 + S^{12} H_2^1 H_1^1) + \frac{\lambda_{S21}}{2} (S^2 H_1^2 H_2^1 + S^{12} H_1^1 H_2^1),
\]

where

\[
V_0 = \mu_1^2 |H_1|^2 + \lambda_1 |H_1|^4 + \mu_2^2 |H_2|^2 + \lambda_2 |H_2|^4 + \mu_3^2 |S|^2 + \lambda_3 |S|^4 + \lambda_{S1} |S|^2 |H_1|^2 + \lambda_{S2} |S|^2 |H_2|^2 + \lambda_{S3} |H_1|^2 |H_2|^2 + \lambda_4 (H_1^1 H_2^1)(H_2^1 H_1^1).
\]

3 Relic density computation

3.1 Evolution equations

The derivation of the equations for the number density of two DM particles is based on standard assumptions: 1) all particles of the same sector are in thermal equilibrium b) particles of the dark sectors have the same kinetic temperature as those of the SM c) the number densities of DM particles can differ from the equilibrium values when the number density of DM particles times their annihilation cross section becomes too low to
keep up with the expansion rate of the Universe. The different processes that influence the number densities of DM include the annihilation and co-annihilation processes in each sector \( \phi_a \phi^*_b \rightarrow XX \), the DM conversion processes \( \phi_a \phi_b \rightarrow \phi_\gamma X \), and the semi-annihilation processes \( \phi_a \phi_b \rightarrow \phi_\gamma X \). Here \( X \) denotes any SM particle and \( \phi_a \) stands for any particle in the dark sectors. The equation for the number densities, \( n_a \) of DM particles in sector 1 and 2 reads

\[
\frac{dn_a}{dt} = -\sigma_v^{a000}(n^2_a - \bar{n}_a^2) - \sigma_v^{aab0}(n^2_a - \bar{n}_a\bar{n}_b) - \sigma_v^{aab}(n^2_a - \bar{n}_a\bar{n}_b) - \frac{1}{2}\sigma_v^{a0ab}(n_a - \bar{n}_a n_a) - \frac{1}{2}\sigma_v^{aab0}(n^2_a - n_a\bar{n}_b) - \frac{1}{2}\sigma_v^{aab}(n_a n_b - n_a\bar{n}_b) - \frac{3}{2}\sigma_v^{aabb}(n_a n_b - n_a\bar{n}_b) - 3Hn_a \tag{5}
\]

Here \( b \) denotes DM sector different from \( a \) (\( a \neq b \)), \( \bar{n}_a \) and \( \bar{n}_b \) denote the equilibrium number densities of particles in the two dark sectors. The label 0 is used for SM particles, \( \sigma_v^{abcd} \) means the thermally averaged cross section defined as

\[
\sigma_v^{abcd}(T) = \frac{T}{8\pi^4\pi_a(T)\pi_b(T)} \int ds\sqrt{s}K_1\left(\frac{\sqrt{s}}{T}\right) \sum_{\alpha\epsilon a, \beta\epsilon b, \gamma\epsilon c, \delta\epsilon d, \text{pol.}} p^2_{\alpha\beta}\sigma_{\alpha\beta\gamma\delta}(s), \tag{6}
\]

\[
\pi_a(T) = \frac{T}{2\pi^2} \sum_{\alpha\epsilon a} g_{\alpha} m_{\alpha}^2 K_2\left(\frac{m_{\alpha}}{T}\right), \tag{7}
\]

Here \( \sigma_{\alpha\beta\gamma\delta} \) is the cross section for the process \( \phi_a \phi_b \rightarrow \phi_\gamma \phi_\delta \), \( K_1 \), \( K_2 \) are modified Bessel functions of the second kind, and \( m_\alpha \) and \( g_\alpha \) stand for the mass and the number of degrees of freedom of particle \( \phi_\alpha \). Roman indices take the value 0, 1, 2 and Greek indices are used to designate particles in a given sector. The inverse reactions are related via the detailed balance equation

\[
\bar{n}_a\bar{n}_b\sigma_v^{abcd} = \bar{n}_c\bar{n}_d\sigma_v^{cdab}. \tag{8}
\]

Note that in a particular model, only a subset of all possible \( 2 \rightarrow 2 \) processes for DM annihilation listed in Table 2 will be allowed, and only the relevant terms will be included in Eq. (5) by micrOMEGAs.

Usually the DM evolution equations are solved in terms of the abundance, \( Y_a = n_a/s \), where \( s \) is the entropy density. The equation for entropy conservation

\[
\frac{ds}{dt} = -3Hs \tag{9}
\]

allows to convert the time evolution equation into an evolution with respect to the entropy density. Introducing \( \Delta Y_a = Y_a - \bar{Y}_a = \frac{n_a - \bar{n}_a}{s} \), Eq. (5) takes the simple form

\[
3H \frac{d\Delta Y_a}{ds} = -C_a + A_{ab}(s)\Delta Y_b + Q_{ab}(s)\Delta Y_b\Delta Y_c, \tag{10}
\]

\(^2\text{Note that 3-body final states from virtual W and Z exchange are also included in the annihilation (coannihilation) processes entering the thermally averaged cross section by setting the switches VWdecay, VZdecay = 1(2).\)
where

\[ C_a = 3H \frac{dY_a}{ds}, \]  
\[ A_{aa} = Y_a \left( 2(\sigma_{aa00}^0 + \sigma_{aab}^0 + \sigma_{aabb}^0) + \frac{1}{2}(\sigma_{aa00}^0 + \sigma_{aabb}^0) \right) \]  
\[ + \frac{1}{2} Y_b \left( \sigma_{aab0}^0 + \sigma_{aabb}^0 + \frac{1}{2} \sigma_{aabb}^0 \right) \]  
\[ A_{ab} = Y_a \left( \frac{1}{2} \sigma_{abaa}^0 + \frac{1}{2} \sigma_{abbb}^0 + \frac{1}{2} \sigma_{aab0}^0 \right) - Y_b \left( 2\sigma_{abaa}^0 + \sigma_{abba}^0 \right) \]  
\[ Q_{aaa} = \frac{1}{2} (\sigma_{abbb}^0 + \sigma_{aab0}^0 - \sigma_{abaa}^0) \]  
\[ Q_{aab} = 0 \]  
\[ Q_{abb} = -\sigma_{abaa}^0 - \frac{1}{2} \sigma_{abbb}^0 - \frac{1}{2} \sigma_{abba}^0 \]  

Here as above \( b \neq a \). Since \( s \) is a known function of temperature \( T \), Eq. (10) is actually the temperature evolution equation.

### 3.2 Solution of equations

At temperatures larger than the masses of DM particles \( Y_a \) is constant and represents the fraction of total degrees of freedom for each dark sector. Since it is constant, \( C_a = 0 \), and the solution of Eq. (10) is \( \Delta Y_a = 0 \), which means that the DM particles are in thermal equilibrium with SM particles. Note that we make the approximation that \( \Delta Y \ll \bar{Y} \) such that terms in \( \Delta Y_j \Delta Y_k \) in Eq. (10) are neglected. Small deviations from equilibrium are obtained by solving

\[ \Delta Y(s) = A^{-1}(s)C(s). \]  

The numerical solution of Eq. (10) used in the case of one component DM needs to be adapted, the problem is caused by a very small step size in the integration routine. In the region where the linear term dominates, the step of the integration over \( \log(s) \) is about \( \frac{H}{sA} \) leading to a very small step size when \( T \approx M_{cdm} \). To bypass this problem in the one component DM case, we used the approximation (18) until

\[ \Delta Y_i \approx 10^{-2}\bar{Y} \]  

At this point we switch to the numerical solution using the standard Runge-Kutta method. For two components DM, the matrix \( A_{ij} \) has two eigenstates. When there is a noticeable mass difference between the two DM particles, the freeze-out of the heavy component occurs much before that of the light one. Thus we have a region of temperatures where the approximation (18) does not apply because the eigenvalue of one of the eigenstate of \( A \) is small, however the direct numerical integration stalls because the large eigenvalue forces a very small step of integration. In fact it means that the space of solutions has an attractor line. Equations which pose such numerical problems are known as stiff equations. To solve such equations the backward scheme is used. In this scheme at each
step of integration one evaluates derivatives at the final point of the step rather than
at the initial point as in the standard scheme. In micrOMEGAs we use the Rosenbrock
algorithm \[37\] \[38\] for solving stiff equations. This method finds a solution for points where
the standard Runge-Kutta method fails. In the current version we use the Fortran code
presented in \[38\].

To speed up the calculation we first tabulate different cross sections as a function of the
temperature in the interval $T \in [T_{\text{end}}, T_{\text{start}}]$, where $T_{\text{start}}$ is the temperature for which
the condition Eq. 19 is satisfied after solving Eq. 18 and $T_{\text{end}} = 10^{-3}\text{GeV}$. Functions
which interpolates the tabulated data are accessible to the user after the calculation of
the relic density. These functions have the generic name $v_{ijkl}(T)$ where $i, j, k, l$ can
take the value $0, 1, 2$ and $0 \leq i \leq j, k \geq l$. The temperature dependence of the equilibrium
abundances can also be called by the user, the functions are named $Y_{1}(T)$ and $Y_{2}(T)$
and are defined only in the interval $T \in [T_{\text{end}}, T_{\text{start}}]$.

4 Two DM models in micrOMEGAs

In previous versions of micrOMEGAs \[39\] \[40\] we assumed that the names of all particles
transforming non-trivially under the discrete symmetry group started with ‘~’. In the
current version we need to distinguish the particles with different transformation prop-
ties with respect to the discrete group, that is particles belonging to different ’dark’
sectors. For this we use the convention that the names of particles in the second ’dark’
sector starts with ‘~~’. Note that micrOMEGAs does not check the symmetry of the La-
grangian, it assumes that the name convention correctly identifies all particles with the
same discrete symmetry quantum numbers.

Before evaluating DM observables in micrOMEGAs one needs to call the initialization
routine

- sortOddParticles(name)

which fills the global parameters presented in Table 2. Note that there is no restriction on
the relative values of $\text{M}_{\text{cdm1}}$ and $\text{M}_{\text{cdm2}}$, either can be the lightest one. This micromegas4.\,X
version also works for models with only one DM candidate. In this case $\text{CDM1}$ or $\text{CDM2}$
(depending on the name convention chosen by the user) will be initialized by NULL
in C and a blank string in Fortran. The corresponding mass will be set to zero. The
return parameter $\text{name}$ contains the name of the lightest particle and $\text{M}_{\text{cdm}}$ its mass. If
micrOMEGAs gets NAN while evaluating constraints, then $\text{name}$ contains the name of the
problematic constraint and sortOddParticles returns an error code.

| Name   | units | comments                                      |
|--------|-------|-----------------------------------------------|
| CDM1   | character | name of the lightest particle in first DM sector |
| CDM2   | character | name of the lightest particle in second DM sector |
| $\text{M}_{\text{cdm1}}$ | GeV   | Mass of CDM1                                  |
| $\text{M}_{\text{cdm2}}$ | GeV   | Mass of CDM2                                  |
| $\text{M}_{\text{cdm}}$ | GeV   | $\min(M_{\text{cdm1}}, M_{\text{cdm2}})$ if both exist |
There are two functions for the evaluation of the relic density. The new routine
\texttt{darkOmega2(fast, Beps)}
calculates $\Omega h^2$ for both one- and two-components DM models. The parameter \texttt{fast=1} flag forces the fast calculation (for more details see Ref. \cite{39}). This is the recommended option and gives an accuracy around 1%. The parameter \texttt{Beps} defines the criteria for including a given coannihilation channel in the computation of the thermally averaged cross-section. \cite{39}. The recommended value is $\texttt{Beps}=10^{-4} - 10^{-6}$, if \texttt{Beps}= 1 only anni-

\texttt{hilation of the lightest odd particle is computed. darkOmega2} also calculates the global parameter $\texttt{fracCDM2}$ which represents the mass fraction of CDM2 in the total relic density

\begin{align}
\Omega &= \Omega_1 + \Omega_2 \\
\text{fracCDM2} &= \frac{\Omega_2}{\Omega}
\end{align}

This parameter is then used in routines which calculate the total signal from both DM candidates in direct, indirect and neutrino telescope experiments, \texttt{nucleusRecoil, calcSpectrum,} and \texttt{neutrinoFlux}. The user can change the global \texttt{fracCDM2} parameter before the calculation of these observables to take into account the fact that the value of the dark matter fraction in the Milky Way could be different than in the early Universe.

The \texttt{darkOmega} function is the same as in previous versions and is appropriate for models with only one dark matter candidate since it does not distinguish the classes of the discrete symmetry group. For example it will assume that all particles whose name starts with one or two tildes belong to the same dark sector and are in thermal equilibrium. This is in general not the case if the discrete symmetry distinguishes two dark matter sectors. The \texttt{darkOmega} function should therefore be used only for models with one dark matter sector.

The DM nucleon amplitude and cross section relevant for direct detection is computed for each DM candidate with the help of the routine
\texttt{nucleonAmplitudes( CDM, qBOX,pAsi,pAsd,nAsi,nAsd)}
where the first parameter is the name of DM particles. All other parameters have the same meaning as in previous versions. Here there is no rescaling to account for the dark matter fraction of each component.

The \texttt{micrOMEGAs} routines for model independent analyses contained in the \texttt{mdlIndep} directory do not take into account the possibility of two DM particles. These routines depend only on the global parameter $M_{cdm}$. All facilities of previous versions of \texttt{micrOMEGAs} \cite{41} are included in this version except for the option to compute the relic density and DM observables when there is an initial DM $\rightarrow$ DM asymmetry. A complete list of \texttt{micrOMEGAs} routines is provided in the manual contained in the \texttt{man} directory.

5 Example

As an example we will consider an extension of the SM with two Higgs doublets and a singlet and a discrete $Z_4$ symmetry \cite{34}. The potential of the model is given in Eqs. (4, 3), the independent parameters are chosen as the masses of the scalars $M_h, M_H, M_S, M_{H^0}, M_{A^0}$ and 8 of the $\lambda_i$’s, see Table \texttt{3}. The first dark sector contains only $S$ while the dark sector 2 contains the doublet $H_0, A^0, H^\pm$, with either $H^0$ or $A^0$ as the possible dark matter. For the set of input parameters defined in Table \texttt{3} The evolution of the abundance for the
two dark matter candidates $S, H$ is illustrated in Figure 5. Furthermore the abundances are compared with the case where DM conversion and/or semi-annihilation is ignored.

Table 3: Input parameters of $Z_4$ model

| Name | Value | Name | Value | Name | Value |
|------|-------|------|-------|------|-------|
| $M_h$ | 125.89 | $m_h$ | | $\lambda_2$ | 0.8162 |
| $M_{sc}$ | 578.0 | $m_{sc}$ | | $\lambda_3$ | -0.1723 |
| $M_{HX}$ | 895.5 | $m_{HX}$ | | $\lambda_S$ | 1.9121 |
| $M_{H3}$ | 900.6 | $m_A$ | | $\lambda'_S$ | 1.017 |
| $M_{HC}$ | 895.64 | $m_{H+}$ | | $\lambda_{S1}$ | 0.2367 |
| | | | | $\lambda_{S2}$ | -1.139 |
| | | | | $\lambda_{S12}$ | 0.7629 |
| | | | | $\lambda_{S21}$ | -0.2054 |

Figure 1: Abundance ($Y_i$) as a function of $x = M_{CDM1}/T$ for each DM particle in the doublet and singlet $Z_4$ model when including all channels (full), only annihilation channels (dash), and also semi-annihilation channels (dot). Note that for CDM1 (left plot), adding semi-annihilation channels induces only a few percent variation in the abundance.

Running micrOMEGAs for the benchmark point of Table 3 (bench3.par) with the options MASSES_INFO, OMEGA, INDIRECT_DETECTION, DIRECT_DETECTION and the switches VWDECAY=1, VZDECAY=1 will lead to the following output

Dark matter candidate is ‘~sc’ with spin=0/2 mass=5.78E+02
Dark matter candidate is ‘~~X’ with spin=0/2 mass=8.96E+02

=== MASSES OF HIGG AND ODD PARTICLES: ===
Higgs masses and widths
   h  125.89 4.26E-03

Masses of odd sector Particles:
   ~sc : M_{sc} = 578.0 || ~~~X : M_{HX} = 895.5 || ~~~H^+ : M_{HC} = 895.6
   ~~~H3 : M_{H3} = 900.6 ||
==== Calculation of relic density ====
\omega_1 = 5.91 \times 10^{-2}
\omega_2 = 6.14 \times 10^{-2}

==== Indirect detection ======

| Channel | \text{vcs \text{[cm}^3\text{/s]} |\n|-----------------|------------------|
| \text{annihilation cross section} | 5.89 \times 10^{-26} \text{ cm}^3\text{/s}|
| \text{contribution of processes} | |

\text{annihilation cross section} 5.89 \times 10^{-26} \text{ cm}^3\text{/s}
\text{contribution of processes}

\sim \text{sc}, \sim \text{X} \rightarrow \text{Z} \sim \text{Sc} 1.83 \times 10^{-1}
\sim \text{sc}, \sim \text{X} \rightarrow \text{Z} \sim \text{sc} 1.83 \times 10^{-1}
\sim \text{X}, \sim \text{X} \rightarrow \text{W}^+ \text{W}^- 7.47 \times 10^{-2}
\sim \text{sc}, \sim \text{sc} \rightarrow \text{W}^- \sim \text{H}^+ 7.24 \times 10^{-2}
\sim \text{sc}, \sim \text{X} \rightarrow \text{W}^+ \sim \text{H}^- 7.24 \times 10^{-2}
\sim \text{sc}, \sim \text{X} \rightarrow \text{h} \sim \text{Sc} 6.15 \times 10^{-2}
\sim \text{sc}, \sim \text{X} \rightarrow \text{h} \sim \text{sc} 6.15 \times 10^{-2}
\sim \text{X}, \sim \text{X} \rightarrow \text{Z} \sim \text{X} 5.20 \times 10^{-2}
\sim \text{sc}, \sim \text{sc} \rightarrow \text{W}^+ \text{W}^- 3.95 \times 10^{-2}
\sim \text{sc}, \sim \text{sc} \rightarrow \text{Z} \sim \text{X} 2.82 \times 10^{-2}
\sim \text{sc}, \sim \text{sc} \rightarrow \text{Z} \sim \text{X} 2.82 \times 10^{-2}
\sim \text{sc}, \sim \text{X} \rightarrow \text{h} \sim \text{H} 2.30 \times 10^{-2}
\sim \text{sc}, \sim \text{X} \rightarrow \text{h} \sim \text{H} 2.30 \times 10^{-2}
\sim \text{sc}, \sim \text{X} \rightarrow \text{Z} \sim \text{H} 1.96 \times 10^{-2}
\sim \text{sc}, \sim \text{X} \rightarrow \text{h} \sim \text{h} 1.91 \times 10^{-2}
\sim \text{X}, \sim \text{X} \rightarrow \text{h} \sim \text{h} 1.09 \times 10^{-2}
\sim \text{sc}, \sim \text{sc} \rightarrow \text{Z} \sim \text{H} 8.50 \times 10^{-3}
\sim \text{sc}, \sim \text{sc} \rightarrow \text{Z} \sim \text{H} 8.50 \times 10^{-3}
\sim \text{sc}, \sim \text{sc} \rightarrow \text{h} \sim \text{X} 7.27 \times 10^{-3}
\sim \text{sc}, \sim \text{X} \rightarrow \text{h} \sim \text{X} 7.27 \times 10^{-3}
\sim \text{sc}, \sim \text{sc} \rightarrow \text{W}^+ \sim \text{H}^- 5.57 \times 10^{-3}
\sim \text{sc}, \sim \text{sc} \rightarrow \text{W}^- \sim \text{H}^+ 5.57 \times 10^{-3}
\sim \text{sc}, \sim \text{sc} \rightarrow \text{t} \text{T} 3.85 \times 10^{-3}
\sim \text{X}, \sim \text{X} \rightarrow \text{t} \text{T} 8.32 \times 10^{-4}

\text{sigmav} = 5.89 \times 10^{-26} \text{[cm}^3\text{/s]}

Photon flux for angle of sight \( f = 0.10 \text{[rad]} \)
and spherical region described by cone with angle 0.10[rad]

\text{Photon flux} = 2.13 \times 10^{-16} \text{[cm}^2 \text{sr s GeV}]^{-1} \text{ for } E = 289.0 \text{[GeV]}

\text{Positron flux} = 1.01 \times 10^{-14} \text{[cm}^2 \text{sr s GeV}]^{-1} \text{ for } E = 289.0 \text{[GeV]}

\text{Antiproton flux} = 1.75 \times 10^{-13} \text{[cm}^2 \text{sr s GeV}]^{-1} \text{ for } E = 289.0 \text{[GeV]}

==== Calculation of CDM-nucleons amplitudes ====

\text{CDM[antiCDM]-nucleon micrOMEGAs amplitudes for } \sim \text{sc}

\text{proton: SI } 1.813 \times 10^{-9} \text{ [1.813 \times 10^{-9}]} \text{ SD } 0.000 \times 0.000 \text{ [0.000 \times 0.000]}
\text{neutron: SI } 1.831 \times 10^{-9} \text{ [1.831 \times 10^{-9}]} \text{ SD } 0.000 \times 0.000 \text{ [0.000 \times 0.000]}
CDM[antiCDM]-nucleon cross sections [pb]:
  proton SI 1.433E-09 [1.433E-09] SD 0.000E+00 [0.000E+00]
  neutron SI 1.461E-09 [1.461E-09] SD 0.000E+00 [0.000E+00]
CDM[antiCDM]-nucleon micrOMEGAs amplitudes for ~X
  proton: SI -8.929E-10 [-8.929E-10] SD 0.000E+00 [0.000E+00]
  neutron: SI -9.017E-10 [-9.017E-10] SD 0.000E+00 [0.000E+00]
CDM[antiCDM]-nucleon cross sections [pb]:
  proton SI 3.473E-10 [3.473E-10] SD 0.000E+00 [0.000E+00]
  neutron SI 3.543E-10 [3.543E-10] SD 0.000E+00 [0.000E+00]

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Appendix

As another example of a two-component DM model, we consider a model that contains two singlets $S_1$ and $S_2$ in addition to the SM Higgs doublet, $H$. We impose a $Z_5$ discrete symmetry with $X_H = 0$, $X_{S_1} = 1/5$ and $X_{S_2} = -3/5$. The potential reads

$$V_{Z_5} = V_0 + \frac{\lambda_{31}}{2} (S_1^3 S_2 + S_1^3 S_2^\dagger) + \frac{\lambda_{32}}{2} (S_2^3 S_1 + S_2^3 S_1^\dagger) + \frac{\mu_{SS_1}}{2} (S_1^2 S_2^\dagger + S_1^2 S_2) + \frac{\mu_{SS_2}}{2} (S_1 S_2 + S_1^\dagger S_2^\dagger),$$

(22)

where

$$V_0 = \mu_1^2 |H|^2 + \lambda_1 |H|^4 + \mu_{S_1}^2 |S_1|^2 + \mu_{S_2}^2 |S_2|^2 + \lambda_{41} |S_1|^4 + \lambda_{42} |S_2|^4 + \lambda_{412} |S_1|^2 |S_2|^2 + \lambda_{S_1} |S_1|^2 |H|^2 + \lambda_{S_2} |S_2|^2 |H|^2$$

(23)

is the part of the potential valid for any choice of discrete symmetry $Z_N$. The input parameters of the model are the masses $M_h, M_{S_1}, M_{S_2}$ and the couplings $\lambda_{41}, \lambda_{42}, \lambda_{412}, \lambda_{31}, \lambda_{32}, \lambda_{S_1}, \lambda_{S_2}, \mu_{SS_1}, \mu_{SS_2}$. This model features only one particle in each of the dark sector and includes interactions between the two dark sectors that were not present in the $Z_4$ model considered in section 5 for example $S_1 S_1 \rightarrow S_1 S_2$. This model is provided in the directory $Z5M$ together with the Lanhep source code to create the appropriate CalcHEP model files.

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