WHERE THE BLUE STRAGGLERS ROAM: SEARCHING FOR A LINK BETWEEN FORMATION AND ENVIRONMENT

NATHAN LEIGH AND ALISON SILLS
Department of Physics and Astronomy, McMaster University, Hamilton, ON L8S 4M1, Canada; leighn@mcmaster.ca, asills@mcmaster.ca

AND

CHRISTIAN KNIGGE
School of Physics and Astronomy, Southampton University, Highfield, Southampton SO17 1BJ, UK; christian@astro.soton.ac.uk

Received 2006 November 28; accepted 2007 February 13

ABSTRACT

The formation of blue stragglers is still not completely understood, particularly the relationship between formation environment and mechanism. We use a large, homogeneous sample of blue stragglers in the cores of 57 globular clusters to investigate the relationships between blue straggler populations and their environments. We use a consistent definition of "blue straggler" based on position in the color-magnitude diagram and normalize the population relative to the number of red giant branch stars in the core. We find that the previously determined anticorrelation between blue straggler frequency and total cluster mass is present in the purely core population. We find some weak anticorrelations with central velocity dispersion and with half-mass relaxation time. The blue straggler frequency does not show any trend with any other cluster parameter. Even though collisions may be expected to be a dominant blue straggler formation process in globular cluster cores, we find no correlation between the frequency of blue stragglers and the collision rate in the core. We also investigated the blue straggler luminosity function shape and found no relationship between any cluster parameter and the distribution of blue stragglers in the color-magnitude diagram. Our results are inconsistent with some recent models of blue straggler formation that include collisional formation mechanisms and may suggest that almost all observed blue stragglers are formed in binary systems.

Subject headings: blue stragglers — globular clusters: general

1. INTRODUCTION

Blue stragglers are stars that are brighter and bluer (hotter) than the main-sequence (MS) turnoff. Such stars have the same mass but seemingly missed their peers’ cue to make the transition to lower temperatures, having already evolved off the MS and begun their ascent up the giant branch (GB). First discovered by Sandage (1953) in the cluster M3, blue straggler stars (BSSs) are an example of the inability of standard stellar evolution alone to explain all stars, and are used as the prime example of the complex interplay between stellar evolution and stellar dynamics (e.g., Sills et al. 2005). Numerous formation mechanisms have been proposed over the years, but the currently favored mechanisms are thought to depend on cluster dynamics.

There is a consensus that blue stragglers are the products of stellar mergers between two (or more) low-mass MS stars, through either direct stellar collisions or the coalescence of a binary system (Leonard 1989; Livio 1993; Stryker 1993; Bailyn 1995). In order for a binary system to coalesce, Roche lobe overflow must occur, triggering mass transfer from the outer envelope of an evolved donor onto that of its companion. As such, the process is dependent on the donor’s evolutionary state. Collisions, on the other hand, do not depend as much on the evolutionary status of the participants since in this case two (or more) stars pass very close to one another, form a brief and highly eccentric binary system, and then rapidly spiral inward and merge as tidal forces dissipate the orbital energy.

The evidence suggests that both formation mechanisms do occur, although the preferred creation pathway appears dependent on the cluster environment (e.g., Warren et al. 2005; Mapelli et al. 2006). Observations from the Hubble Space Telescope (HST) indicate that BSSs are centrally concentrated in globular clusters (GCs; Ferraro et al. 1999), although they have been detected throughout all the clusters that have been surveyed well. The BSS populations have been found to have a bimodal radial distribution in clusters such as M55 (Zaggia et al. 1997), M3 (Ferraro et al. 1997), and 47 Tuc (NGC 104; Ferraro et al. 2004), with elevated numbers in the cores followed by a “zone of avoidance” at a few core radii and a final rise in BSS numbers toward the cluster outskirts. This bimodal trend is thought to arise because two separate formation mechanisms are dominating in the core and in the cluster periphery, with mass transfer predominantly taking place in the outer, less dense regions and collisions mainly occurring toward the cluster center. In support of this last point, eclipsing binaries consisting of main-sequence components having short periods and sharing a common envelope, called contact or W Ursae Majoris binaries, have been observed among BSSs in globular (Mateo et al. 1990; Yan & Mateo 1994) and open clusters (Ahumada & Lapasset 1995).

There is an additional complication, however, when considering the effects of stellar collisions. It has been suggested that collisions need not only occur between two single stars in exceptionally dense environments but rather might also occur in less dense systems via resonant interactions between primordial binaries (Bacon et al. 1996). Two binary pairs locked in a tightly bound four-body system can actually increase the rate of collisions by increasing the collisional cross section of the system (Fregeau et al. 2004). Indeed, multiple collisions are thought to be responsible for some of the blue stragglers we see, in particular those having masses around twice that of our Sun or more (Sepinsky et al. 2000), or the unusual blue straggler binary system in 47 Tuc, which probably requires three progenitor stars (Knigge et al. 2006). Clearly both cluster dynamics and binary star populations will determine how many of these binary-mediated collisions will occur.
Piotto et al. (2004) recently examined the color-magnitude diagrams (CMDs) of 56 different GCs, comparing the BSS frequency to cluster properties such as total mass (absolute luminosity) and central density. The relative frequencies were approximated by normalizing the number of BSSs to the horizontal branch (HB) or the red giant branch (RGB), although the results did not depend on which specific frequency they chose. They found that the most massive clusters had the lowest frequency of BSSs and that there was little or no correlation between BSS frequency and cluster collisional parameter. They also showed that the BSS luminosity function for the most luminous clusters had a brighter peak and extended to brighter luminosities than did that of the fainter clusters.

The absence of a correlation between BSS frequency and collision number, in particular, is surprising, since other evidence suggests that dynamical interactions do affect stellar populations in GCs. For example, GCs host enhanced numbers of unusual short-period binary systems such as low-mass X-ray binaries (LMXBs; Dieball et al. 2005), cataclysmic variables (CVs; Knigge et al. 2003), and millisecond pulsars (MSPs; Edmonds et al. 2003). These objects, like blue stragglers, are thought to trace the dynamically created populations of clusters. Their presence has been linked to the high densities found in the cores of GCs, which are thought to lead to an increase in the frequency of close encounters and thus in the formation rate of exotic binary systems. Indeed, the number of close binaries in GCs observed in X-rays has been shown to be correlated with the predicted stellar encounter rate of the cluster (Pooley et al. 2003).

A useful quantity for parameterizing the surface brightness distribution of GCs is the core radius, $r_c$, defined as the distance from the cluster center at which the surface brightness is half its central value. That is, at a distance of $r_c$ from the center of a King model globular cluster, the density is expected to have dropped off to around a third of the density at the cluster center (Spitzer 1987). This then implies that the core encloses the densest regions of the cluster by at least a factor of a few, and hence one would expect interactions between stars, specifically collisional processes, to occur with the greatest frequency therein.

In our quest to determine the cluster environment’s effect on BSS formation, we decided to focus solely on the stars found within the core in order to isolate those most likely to undergo stellar encounters. We wanted to search for empirical evidence for collisional BSS formation, and the cores of clusters are the most likely place for collisions not only to occur but also to dominate (Mapelli et al. 2006; Ferraro et al. 2004). Previous attempts to connect blue straggler populations to global cluster properties (Piotto et al. 2004; Davies et al. 2004) did not attempt to focus on a single, homogeneous environment. By concentrating solely on the core, we therefore maintain consistent sampling from cluster to cluster. We note that while directing our attention to the core allows us to isolate an approximately uniform dynamical environment, it also presents a statistical complication in post–core-collapse clusters since these tend to have small core radii and the star counts therein thus tend to be restricted. Fortunately, only a small fraction of the clusters used in this paper have undergone core collapse, so this effect should not have a significant impact on our results.

In this paper, we use Hubble Space Telescope (HST) data to look for possible trends between relative BSS frequency and various cluster parameters, including total cluster mass, central density, and central velocity dispersion as well as collisional parameters. We discuss our data set as well as our methodology for BSS selection in the cluster CMDs in § 2. In § 4 we present our results, including trends in the relative BSS frequencies as well as a comparison of blue straggler luminosity functions (BSLFs). We summarize and discuss our findings in § 6.

2. THE DATA

The color-magnitude diagrams and photometric databases for 74 Galactic globular clusters were used in this paper. The observations, taken from Piotto et al. (2002), were made using the HST’s WFPC2 camera in the F439W and F555W bands, with the PC camera centered on the cluster center in each case. The field of view for each cluster generally contains anywhere from a few thousand to roughly 47,000 stars. Of the 74 potential Galactic GCs, only 57 were deemed fit for analysis, with the remaining 17 having been discarded due to poor reliability of the data at or above the main-sequence turnoff (MSTO) based on the overall appearance of their respective CMDs. Core radii and other cluster parameters were taken from Harris (1996) and Pryor & Meylan (1993).

The data available at the Padova Web site have not been corrected for completeness. This could be a problem for our analysis if we cannot accurately determine the total number of blue stragglers, red giant, horizontal branch, and extended horizontal branch (EHB) stars. However, we do not expect this to be an issue in this paper. All the clusters that we retained in our sample have clearly defined main-sequence turnoffs and subgiant branches. The populations of interest are brighter than the turnoff, by definition, and should be less affected by photometric errors and completeness. We expect that the corrections for the faintest objects that we identify as blue stragglers should be on the order of one star or fewer, which will not change the results of this paper. To be safe, however, stars having sufficiently large errors in $m_{F439}$ and $m_{F555}$, respectively denoted by $\sigma_{F439}$ and $\sigma_{F555}$, were also rejected from our counts if their total error was more than 0.1 mag.

1 The positions of the stars, as well as their magnitudes in both the F439W and F555W bands and the $B$ and $V$ standard Johnson system, can be found at the Padova Globular Cluster Group Web pages at http://dipastro.pd.astro.it/globulars.
We defined a set of boundaries in the color-magnitude diagram for each of our populations of interest: blue stragglers, red giant branch stars, horizontal branch stars, and extended horizontal branch stars. The details of these definitions can be found in the Appendix. The boundaries of our blue straggler selection box were ultimately chosen for consistency. By eliminating potential selection effects such as “by eye” estimates, we were able to minimize the possibility of counting EHB or MSTO stars as BSSs. Moreover, since we are considering relative frequencies and there is a possibility of mistakenly including stars other than BSSs in our counts, it seems prudent that we at least make the attempt to systematically choose stars in all clusters. We are most interested in using the evolved populations to normalize the number of blue stragglers, both to give a sense of photometric error and to remove the obvious relation that clusters with more stars have more blue stragglers. Therefore, we limited ourselves to red giants with the same luminosities as the blue stragglers. These boundaries are shown for NGC 5904 in Figure 1. The full data for all clusters are given in the Appendix.

3. METHODS OF NORMALIZATION

With our sample of core blue straggler, HB, EHB, and RGB stars established consistently from cluster to cluster, it was then necessary to address the issue of normalization. As one might expect, clusters having more stars tend to be home to a larger population of BSSs. Number counts of stars therefore had to be converted into relative frequencies. This was previously done by dividing the number of BSSs by either the number of horizontal branch stars (Piotto et al. 2004),

\[ F_{\text{HB}}^{\text{BSS}} = \frac{N_{\text{BSS}}}{N_{\text{HB}}} \]  

or the total cluster mass (De Marchi et al. 2006),

\[ F_{\text{M}_{\text{tot}}}^{\text{BSS}} = \frac{N_{\text{BSS}}}{M_{\text{tot}}} \]  

Piotto et al. (2004) also looked at using the number of RGB stars for normalization, but after finding similar results, they decided to simply use the HB. The preferred means of normalization is a matter of some debate, and hence we similarly calculated relative frequencies in a few separate ways in order to gauge which is best. Frequencies were normalized

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**Fig. 2.**—Plots of the core BSS frequency vs. the total cluster $V$ magnitude. Frequencies were normalized using RGB stars (bottom right), HB stars (bottom left), EHB stars (top right), and finally, HB and EHB stars combined (top left).
using the HB, the EHB, the HB and the EHB, and the RGB:

\[ F_{\text{HB BSS}} = \frac{N_{\text{BSS}}}{N_{\text{HB}}}, \quad (3) \]

\[ F_{\text{EHB BSS}} = \frac{N_{\text{BSS}}}{N_{\text{EHB}}}, \quad (4) \]

\[ F_{\text{HB+EHB BSS}} = \frac{N_{\text{BSS}}}{N_{\text{HB}} + N_{\text{EHB}}}, \quad (5) \]

\[ F_{\text{RGB BSS}} = \frac{N_{\text{BSS}}}{N_{\text{RGB}}}. \quad (6) \]

Plotting these frequencies against the total \( V \) magnitude, previously shown to exhibit a clear anticorrelation (Piotto et al. 2004), proved that using the RGB gives us the tightest relationship. This reduction of scatter was similarly observed upon comparing the BSS frequency to other cluster parameters such as the central surface brightness, the central velocity dispersion, and the collisional rate. Figure 2 shows the BSS frequency versus the total absolute \( V \) magnitude of the cluster for all four normalization methods.

4. RESULTS

Having obtained the numbers and frequencies of blue stragglers in the cluster cores, we attempted to determine correlations between the blue straggler frequency and global cluster properties such as total mass, velocity dispersion, core density, etc. If the preferred BSS formation mechanism in the core is direct stellar collisions, then we should see a link between clusters with higher instances of collisions and more pronounced BSS populations; if the formation mechanism is not collisions, we would still expect to see a relationship between the properties of the cluster and its stellar populations.

The central surface brightness and the core radius were taken from Harris (1996). Values for the central velocity dispersion were taken from Pryor & Meylan (1993). Any other parameters, including the central density and the total absolute luminosity, came from Piotto et al. (2002) with the exception of the normalized cluster ages, which were taken from De Angeli et al. (2005) and for which the Zinn & West (1984) metallicity scale values were employed. Error bars for all plots were calculated assuming Poisson statistics.
It should be noted here that while the number of blue straggler stars in a core is a tracer of the total number of stars in the core, as well as of the total number of HB and RGB stars, we found no correlation between the number of blue stragglers and the number of EHB stars. It has been speculated (Ferraro et al. 2003) that there might be a connection between BSS and EHB populations. The trend in that paper (of six clusters) was that clusters either had bright blue stragglers or EHB stars, but not both. With this larger self-consistent sample, we do not find the same result. The number of EHB stars seems to be completely independent of how many bright blue stragglers exist in the cluster.

Relative frequencies appeared independent of the majority of the cluster parameters analyzed, with a couple of noteworthy exceptions. One trend observed was that the least massive clusters (those having the lowest absolute luminosities) had the highest relative frequencies of blue stragglers, and vice versa. This anticorrelation was previously observed by Piotto et al. (2004), although their choice of BSS selection and chosen method of normalization arguably led to a greater degree of scatter in their plots. According to our analysis, using the HB for normalization yielded correlations that were overall not as tight as those made using the RGB. They also did not distinguish between blue stragglers inside or outside one core radius but simply counted the stars in their observed fields. Given the bimodality of the observed BSS radial distribution in some GCs, this could have resulted in the inclusion of BSSs that were never subject to the same dynamical conditions as those BSSs found in the core.

A similar anticorrelation was found between $F_{\text{BSS}}$ and the central velocity dispersion, shown in Figure 3. This is perhaps unsurprising, since velocity dispersion is known to be correlated with cluster mass (Djorgovski & Meylan 1994). The blue straggler frequencies showed no clear dependence on any other cluster parameters, including the central density, the central surface brightness, and the cluster age.

Figure 4 shows the blue straggler frequency versus the core and half-mass relaxation times. While weak anticorrelations were found with both the core and half-mass relaxation times, $F_{\text{BSS}}$ was found to show a stronger anticorrelation with the latter. Moreover, it seems as though the distribution begins to flatten out at higher $\log t_c$, specifically beyond around 10$^6$ yr.

We also considered the brightest blue stragglers (BBSSs) separately, under the assumption that these stars are most likely to be collision products. Figure 2 of Monkmann et al. (2006) shows that, in the case of 47 Tuc (NGC 104), the number of bright blue stragglers falls off noticeably outside the cluster core. These brightest blue stragglers found only within the core have a $B$ magnitude of less than about 15.60 mag or a $V$ magnitude of less than about 15.36 mag. Assuming the BBSSs in other clusters are similar to those found in 47 Tuc, we defined the brightest BSSs as those having a $V$ magnitude of 1.74 mag brighter than that of the MSTO. As illustrated in Figure 5, the usual trends with $M_V$ and the central velocity dispersion were found. No new trends between the BBSS relative frequencies and any cluster parameters emerged.

We also looked at the relative BSS frequencies in only the most massive clusters for which $M_V < -8.8$ under the assumption of Davies et al. (2004) that the BSSs in these clusters should predominantly be collision products. Collisional BSSs are thought to be brighter than those formed from primordial binaries. As illustrated in Figure 6, no trends were found between BSS relative frequencies and any cluster parameters when clusters with $M_V > -8.8$ were ignored. Indeed, the previously established trend between $M_V$ and $F_{\text{BSS}}$ is considerably weakened by eliminating clusters with $M_V > -8.8$.

BSS frequencies were also plotted against a parameter used to approximate the rate of stellar collisions per year. Following Pooley & Hut (2006),

$$\Gamma = \frac{\rho_0^2 \Gamma_c^3}{\sigma_0},$$

where $\rho_0$ is the central density in units of solar luminosity per cubic parsec, $\sigma_0$ is the central velocity dispersion in kilometers per second and $r_c$ is the core radius in parsecs. If there is a tight correlation between the fraction of blue stragglers and $\Gamma$, then we can conclude that direct stellar collisions are responsible for most of the blue stragglers in cluster cores. Figure 7 shows, if anything, a decline in BSS frequency with increasing collisional rate. This weak anticorrelation is likely not an artifact of the more populous clusters having more stars available to undergo collisions since we are dealing with normalized BSS frequencies as opposed to pure number counts. This anticorrelation has been seen by Piotto et al. (2004) and Sandquist (2005) for blue straggler populations from a larger region of the cluster. The trend is weak, and one could argue that there is no correlation.

An additional comparison can be made to the probability that a given star will undergo a collision in 1 yr, denoted by $\gamma$. We divide the rate of stellar collisions by the total number of stars in the cluster core, $N_{\text{star}}$, found by directly counting them in the database of Piotto et al. (2002) and then multiplying by the appropriate geometrical correction factor. In order for our counts to be representative of the entire core, it was necessary to extrapolate our results in the case of clusters for which only a fraction of the core was sampled. Therefore, the total number of stars was multiplied by the ratio of the entire core area to that of the sampled region in each cluster. Figure 7 clearly shows that there is no dependence of $F_{\text{BSS}}$ on $\gamma$. Similar results were also found when we used the collisional parameter given in Piotto et al. (2004). We also looked for connections between both $\Gamma$ and $\gamma$ and the brightest...
blue stragglers, and the blue stragglers in the brightest clusters. We found no trend in either case.

To quantify these dependences or lack thereof, we calculated the Spearman correlation coefficients (Press et al. 1992; Wall & Jenkins 2003) between the blue straggler frequency and a variety of cluster parameters. The results are given in Table 1. The correlation coefficient $r_s$ ranges from 0 (no correlation) to 1 (completely correlated) or to $-1$ (completely anticorrelated). Column (3), labeled “Probability,” gives the chance that these data are uncorrelated. Clearly the most important anticorrelations are with the total cluster magnitude and the central velocity dispersion (the Spearman coefficient for $M_V$ is positive for an anticorrelation because the magnitude scale is backward). The anticorrelation with half-mass relaxation time also shows up here, and the frequency of blue stragglers in clusters may also be anticorrelated with the core relaxation time and collision rate, although this is not conclusive from these data.

5. BLUE STRAGGLER LUMINOSITY FUNCTIONS

Having investigated the relationship between the frequency of blue stragglers and their host cluster properties, we now turn to look at the details of the blue straggler population itself. Cumulative blue straggler luminosity functions (BSLFs) were made for all 57 clusters in our sample. The magnitude of the MSTO differs from cluster to cluster and so, in order to correct for these discrepancies, it was subtracted from the BSS magnitudes in each cluster.

We wanted to quantify the shape of these luminosity functions in order to determine whether there were any connections between BSLF shape and global cluster parameters. We found that all the BSLFs could be well fit using a quadratic (but not a linear) function of magnitude. Some examples of the fits are given in the top panel of Figure 8. The fits for all clusters are given in the bottom panel.

We looked at each of the quadratic coefficients as a function of all of the cluster parameters and found that the coefficients had no dependence on any parameter, including total cluster magnitude or metallicity. We were particularly interested in metallicity since the BSLF is a measure of the properties of BSS stellar evolution, which could depend on metallicity. According to these data, it does not.

Piotto et al. (2004) argued that if the BSS formation mechanisms depend on the cluster mass, then one would expect the blue...
straggler LFs to likewise depend on the mass. They predicted that the luminosity distribution of collisionally produced BSSs should differ from those created via mass transfer or the merger of a binary system due to different resulting interior chemical profiles. They were able to generate separate BSLFs for clusters with \( M_V < -8.8 \) and \( M_V > -8.8 \) in support of their hypothesis. Upon subtracting MSTO magnitudes from peak BSLF magnitudes and creating individual BSLFs for clusters above and below a total \( V \) magnitude of \(-8.8\), we found the difference between the two subsets of BSLFs to be negligible. Interestingly, there were in total only 11 clusters in our data set for which \( M_V < -8.8 \), so had we found any potential trends, their reliability would be suspect. Any generalizations made regarding the most massive clusters should be disregarded due to the small number of clusters in the Piotto et al. (2002) data set in this regime.

We repeated this experiment by binning our BSLFs according to cluster magnitude, in bins of size 1 mag. The results are shown in Figure 9. We see no trend in the peak of the BSLF with cluster magnitude. We also tried binning the BSLFs by central density (in bins of size 1 in \( \log \rho \)) and by half-mass relaxation time (in bins of size 0.5 in \( \log t_h \)). Again, we found no trend in the peak magnitude or shape of the luminosity function for any of these parameters. We expect, given our analysis of the shapes of the cumulative BSLFs, that binning by any other cluster parameter will similarly yield no trends. Just to check, we performed a Kolmogorov-Smirnov test on the luminosity functions that were binned by absolute cluster magnitude (those shown in Fig. 9). No pairs of distributions were drawn from the same parent distribution with more than a few percent probability. The closest pair (\( -7 < M_V < -6 \) and \( -9 < M_V < -8 \)) have a 57% probability of being drawn from the same distribution; all other pairs were below the 10% level.

6. SUMMARY AND DISCUSSION

We used the large homogeneous database of \( HST \) globular cluster photometry from Piotto et al. (2004) to investigate correlations of blue stragglers with their host cluster properties. First, we applied a consistent definition of “blue straggler” to all our clusters. We chose the MSTO as our starting point and defined our boundaries based only on its location in the CMD. We also defined the location of horizontal branch and extended horizontal branch stars in the CMD. We looked at a variety of normalizations for our BSS frequencies before determining that using the RGB yielded the plots with the least scatter.
There are disappointingly few strong correlations between the frequency of blue stragglers in the cores of these clusters and any global cluster parameter. We confirm the anticorrelation between the total integrated cluster luminosity and relative BSS frequency found by Piotto et al. (2004); we suggest an anticorrelation with central velocity dispersion based on a high correlation coefficient comparable to that found for the cluster luminosity. At a lower significance are possible anticorrelations with half-mass and core relaxation times.

The relaxation time for a cluster is a measure of how long a system can live before individual stellar encounters become important and the approximation of objects moving in a smooth mean potential breaks down. Globular clusters are the quintessential collisional dynamical systems, since their ages are typically much longer than their relaxation times. It seems sensible that the fraction of blue stragglers, a dynamically created population, should depend on the relaxation times of clusters. The puzzle comes, as usual, in the details. First, we are looking at core blue stragglers, so we might expect the blue straggler fraction to go up with decreasing core relaxation time. The observations do give us this kind of trend, but not a very strong one. We might also expect the blue straggler fraction to depend on the half-mass relaxation time, which is a better measure of the dynamical state of the whole system. The blue straggler fraction does depend on $t_2$ in the way that we expect, but only apparently for systems with short dynamical times. Is blue straggler formation a dynamical process which takes a while to turn on? It seems that might be the case.

If the observed anticorrelation between $F_{BSS}$ and the central velocity dispersion is real, then it follows that random relative motions somehow impede stellar mergers. A similar conclusion can be drawn from the plots of $F_{BSS}$ versus $t_2$ in the event that the speculated anticorrelations are truly representative of the cluster dynamics. Collisional processes therefore seem to somehow interfere with the production of BSSs. If the majority of BSSs are, in fact, the remnants of coalescing binaries then it stands to reason that an increase in the number of close encounters or collisions with other stars could result in the disruption of a larger number of binary systems. On the other hand, if the majority of BSSs are the products of stellar collisions, then it is conceivable that those clusters having the highest collisional frequencies are

![Fig. 7](image1.png)

**Fig. 7.**—Top: Plot of the BSS frequency within the cluster core vs. the rate of stellar collisions per year using eq. (7) as the collisional parameter; $\rho_0$ is the central density in units of solar luminosity per cubic parsec, $v_0$ is the central velocity dispersion in kilometers per second, and $r_c$ is the core radius in parsecs. Bottom: Plot of BSS frequency vs. the probability of a stellar collision occurring within the core in 1 yr. Frequencies were normalized using core RGB stars.

![Fig. 8](image2.png)

**Fig. 8.**—Cumulative BSS luminosity functions. The top panel shows the BSLFs for NGC 104 (47 Tuc) and NGC 7099 (M30; solid lines) along with quadratic fits to those functions (dashed lines). The bottom panel shows the quadratic fits to all cluster BSLFs.

![Fig. 9](image3.png)

**Fig. 9.**—Blue straggler luminosity functions, binned according to total cluster magnitude. Solid line, clusters with $M_V$ between $-6$ and $-7$; dotted line, clusters with $M_V$ between $-7$ and $-8$; dashed line, clusters with $M_V$ between $-8$ and $-9$; dash-dotted line, clusters with $M_V$ between $-9$ and $-10$.

| Table 1: Spearman Correlation Coefficients |
|--------------------------------------------|
| Parameter                          | $r_s$ | Probability |
| Total cluster $V$ magnitude          | 0.76  | 7.2E−12     |
| Central velocity dispersion         | −0.70 | 1.0E−05     |
| Half-mass relaxation time           | −0.53 | 2.5E−05     |
| Core relaxation time                | −0.43 | 1.1E−03     |
| Collision rate                      | −0.41 | 0.02        |
| Surface brightness                  | 0.17  | 0.20        |
| Central density                     | 0.08  | 0.58        |
| Collision probability               | −0.09 | 0.63        |
| Age                                | 0.02  | 0.91        |
the most likely to undergo three- or four-body encounters. As such, clusters having the highest collisional rates could also have, on average, the most massive BSSs, resulting from an increased incidence of multibody mergers. This might then contribute to the observed weak anticorrelation between $F_{\text{BSS}}$ and the collisional rate since clusters having a higher incidence of collisions should consequently have a higher incidence of multibody mergers, resulting in a potentially lower relative BSS frequency. We need more, and more accurate, individual surface gravity measurements of blue stragglers in order to explore the idea that a surplus of more massive BSSs can be found in those clusters with a higher $\Gamma$.

The BSS frequency was found to be nearly uniform with every other cluster parameter, suggesting that all globular clusters of all properties produce the same fraction of blue stragglers. The lack of a dependence of $F_{\text{BSS}}$ on cluster age implies that whatever the preferred mechanism(s) of BSS formation, it occurs in globular clusters of every age with comparable frequencies. It should be noted that this result does not extend to open clusters. There is a clear correlation of blue straggler frequency with cluster age for open clusters between the ages of $10^8$ and $10^{10}$ yr (De Marchi et al. 2006).

Cumulative BSS luminosity functions were analyzed for all 57 GCs. Unlike Piotto et al. (2004) we found no real difference between the BSLFs of the most massive clusters and those of the least massive clusters. In fact, we found no correlation between the shape of the cumulative luminosity function and any other cluster property. These results do not support the notion that different interior chemical profiles cause collisionally produced BSSs to have different luminosities from those created via mass transfer or the coalescence of primordial binaries. It does, however, suggest that either the products of both formation mechanisms cannot be distinguished by their luminosity functions alone or a single formation mechanism is operating predominantly in all environments.

Trends were also looked for in the brightest blue stragglers, since we suspected their enhanced brightnesses to imply a collisional origin. We also looked at the entire core blue straggler population in the most massive clusters (also thought to be predominantly a collisional population). No trends were observed. Therefore, even putatively collisional blue stragglers show no connection to their cluster environment.

What conclusions can we draw from this near-complete lack of connection between blue stragglers and their environment? We approached this project with the idea of looking only at blue stragglers formed through stellar collisions (those in the core, or the brightest blue stragglers in the core). Having found no correlations, we are forced to acknowledge that our prediction that core blue stragglers are predominantly formed through collisions may be incorrect. This is in disagreement with many arguments in the literature. Those arguments range from discussions of probable encounter rates (Hills & Day 1976) to the detailed dynamical simulations of Mapelli et al. (2006). It should be noted that while collisions are not solely responsible for their production, they may still play an important role in BSS formation. Indeed, the fraction of close binaries has been found to be correlated with the rate of stellar encounters in GCs (Pooley et al. 2003). It is becoming increasingly clear that GCs represent complex stellar populations and that detailed models are required in order to accurately track their evolution.

It has also become clear, however, that blue stragglers are an elusive bunch. It appears more and more obvious that there are numerous factors working together to produce the populations that we observe. Even if we limit ourselves to considering only those blue stragglers created through binary mergers, we still need to include the effects of cluster dynamics since the binary populations of clusters will be modified through encounters (e.g., Ivanova et al. 2005). In contrast to what Davies et al. (2004) suggest, we do not feel we can reliably say that the effects of collisions will be to explicitly reduce the binary population in the core. Rather, it is likely that the distribution of periods, separations, and mass ratios will be modified through encounters, but precisely how remains difficult to predict. Indeed, dynamical processes act to reduce the periods in short-period binaries rather than destroy them, with the binaries at the lower end of the period distribution shifting the fastest to even shorter periods (Andronov et al. 2006). At the same time, wider binaries can be destroyed in clusters as a result of stellar interactions. Therefore, models of blue straggler populations need to be reasonably complex. In this paper, we present observational constraints on those models. Blue straggler populations must be approximately constant for clusters of all ages, densities, concentrations, velocity dispersions, etc.; the number of blue stragglers decreases with increasing cluster mass; and the type, or luminosity function, of blue stragglers is apparently completely random from cluster to cluster. That the luminosity function data appear random perhaps should not have been a surprise. The current blue straggler luminosity function is a convolution of the blue straggler mass function and the blue straggler lifetimes.

There is one important cluster property for which we could not perform this analysis—the cluster binary fraction. If those clusters with a high binary fraction also have higher relative BSS frequencies then this might suggest a preferential tendency toward BSSs forming via coalescence. More importantly, such a trend could be indicative of more massive clusters having a higher frequency of binaries of the right type. That is, more massive clusters may be more likely to harbor binary systems with components in the right mass range and with the right separation to form blue stragglers in the lifetime of the cluster. It therefore seems wise to develop our knowledge of the types of binary systems commonly found in GCs, specifically the mass ratios, periods, and separations thereof. Preston & Sneden (2000) suggest that GCs either destroy the primordial binaries that spawn long-period BSS binaries like those observed in the Galactic field or were never home to them in the first place. This statement supports the notion that the majority of BSSs formed in globular clusters are the products of the mergers of close binaries, a claim that is not in disagreement with the results of this paper. Work is required on both the observational and theoretical fronts in order to completely understand this ubiquitous, and frustrating, stellar population.

We would like to thank Piotto et al. (2002) for providing a robust data set with which to explore possible BSS trends. This research has been supported by NSERC.

APPENDIX

STELLAR POPULATION SELECTION CRITERIA

Color-magnitude diagrams are often so cluttered that distinguishing the blue stragglers from ordinary MSTO stars, or even those belonging to the horizontal and extended horizontal branches, can be a challenging and ambiguous task. In looking at the BSS
populations of six different GCs, Ferraro et al. (1997) defined boundaries to separate the BSSs from regular MS stars. Using the MSTO as a point of reference, they shifted the CMD of each cluster to coincide with that of M3 for consistency and then divided the blue straggler population into two separate subsamples: bright BSSs with $m_{555} < 19$ mag and faint BSSs with $19.0$ mag $< m_{555} < 19.4$ mag.

De Marchi et al. (2006) similarly studied 216 open clusters containing a total of 2105 BSS candidates in order to compare the blue straggler frequency and the cluster age, suggesting that at least one of the BSS formation mechanisms requires a much longer timescale to operate in order to make its mark on a stellar population. De Marchi et al. defined their own criteria for the selection of blue stragglers and, in contrast to Ferraro et al. (1997), defined boundaries by shifting the zero-age main sequence (ZAMS) towards brighter $V$ magnitudes and enclosed the resident BSSs with borders above and below.

We chose to take as our starting point the sharpest point in the bend of the MSTO centered on the mass of points that populate the MSTO magnitude range as the blue straggler stars. First, two lines of slope $0.6$ mag above the MSTO (lower in $V$) placed 0.45 mag higher in $m_{439} - m_{555}$ and $0.15$ mag higher in $B - V$, by shifting $w/4$ mag lower in $m_{439} - m_{555}$ and $5W/8$ lower in $m_{555}$, as indicated in equation (A1):

$$B - V = (B - V)_0 - w/4,$$
$$V = V_0 - 5w/8.$$  

(A1) (A2)

This shift ensured that our boundary selection starting point, namely, the outer edge of the MSTO, was nearly identical for every cluster. In order to separate the BSSs from the rest of the stars that populate the region just above the MSTO, we drew two lines of slope $-3.5$ in the $(m_{439} - m_{555}, m_{555})$-plane made to intersect points shifted from $(B - V, V)$. One line was shifted $0.5$ mag lower in $m_{439} - m_{555}$ and $0.1$ mag lower in $m_{555}$ from $(B - V, V)$, whereas the other was shifted $2.0$ mag lower in $m_{439} - m_{555}$ and $0.4$ mag lower in $m_{555}$. These new points of intersection are given by

$$(B - V)_r = (B - V) - 0.5,$$
$$V_r = V - 0.1,$$
$$(B - V)_l = (B - V) - 2.0,$$
$$V_l = V - 0.4.$$  

(A3) (A4) (A5) (A6)

Two further boundary conditions were defined by fitting two lines of slope $5.0$, chosen to be more or less parallel to the fitted ZAMS, one intersecting a point shifted $0.2$ mag higher in $m_{439} - m_{555}$ and $0.5$ mag lower in $m_{555}$ from $(B - V, V)$ (top), and another passing through a point $0.2$ mag lower in $m_{439} - m_{555}$ and $0.5$ mag higher in $m_{555}$ (bottom). These new intersection points are given by

$$(B - V),_{l,b} = (B - V) \pm 0.2,$$
$$V,_{l,b} = V \mp 0.5.$$  

(A7) (A8)

These cuts eliminate obvious outliers and further distinguish BSSs from HB and EHB stars. The methodology used in De Marchi et al. (2006) for isolating BSSs similarly incorporated the ZAMS, although their upper and lower boundaries were ultimately defined differently, as outlined in § 1. Finally, one last cut was made to distinguish BSSs from the EHB, namely, a vertical cut made $0.4$ mag lower in $m_{439} - m_{555}$ than the MSTO.

A similar methodology was used to isolate the RGB stars in the cluster CMDs. We are restricting ourselves to RGB stars in the same magnitude range as the blue straggler stars. First, two lines of slope $-19.0$ in the $(m_{439} - m_{555}, m_{555})$-plane were drawn to intersect the MSTO. In order to place them on either side of the RGB, both lines were shifted $0.6$ mag lower in $m_{555}$, although it was necessary to apply different color shifts. The leftmost boundary was placed $0.15$ mag higher in $m_{439} - m_{555}$, while the rightmost boundary was placed $0.45$ mag higher in $m_{439} - m_{555}$. To fully define our RGB sample, a lower boundary was defined using a horizontal cut made $0.6$ mag above the MSTO (lower in $m_{555}$). The upper boundary, on the other hand, was simply defined to be the lower boundary of the HB. RGB stars must therefore simultaneously satisfy

$$-19.0(B - V)_{RGB} + (V - 0.6) + 19.0[(B - V) + 0.15] < V_{RGB},$$
$$V_{RGB} < -19.0(B - V)_{RGB} + (V - 0.6) + 19.0[(B - V) + 0.45],$$
$$V - 0.6 < V_{RGB},$$
$$V_{RGB} > h + 0.4.$$  

(A9) (A10) (A11) (A12)

Pulling out HB and EHB stars from the cluster CMDs was found to be more difficult than for BSSs and RGB stars due to the awkward shape of the bend as the HB extends down to lower luminosities. Exactly where the HB ends and the EHB begins has always been a matter of some controversy, and so the choice of where to place the boundary was arbitrary but was at least consistent from cluster to cluster.
A vertical boundary was placed 0.5 mag lower in $m_{439} - m_{555}$ than the MSTO to distinguish the end of the HB from the start of the EHB. The centermost part (in absolute magnitude) of the grouping of stars that make up the HB, denoted by $h$, was carefully chosen by eye, and two horizontal borders were subsequently defined 0.4 mag above and below. One more boundary, this time a vertical cut to help distinguish the HB from the RGB, was set 0.3, 0.4, or 0.5 mag higher in $m_{439} - m_{555}$ than the MSTO. The decision of which of these three values of HBshift to use was decided for each cluster based on their individual CMDs. Every star in the CMD that fell to the
left of this vertical boundary and between the horizontal ones was taken to be an HB star, and every star that was not already counted as a BSS or a member of the HB was then taken to be an EHB star. Thus, HB stars, denoted by \((B - V)_{\text{HB}}, V_{\text{HB}}\), must simultaneously satisfy

\[
(B - V)_{\text{HB}} < (B - V) + \text{HB}_{\text{shift}},
\]

\[
h - 0.4 < V_{\text{HB}} < h + 0.4.
\]

Finally, it was necessary to eliminate any very faint EHB stars to avoid including any white dwarfs in our sample. Hence, a final boundary was set 3.5 mag below the lower boundary of the HB. This then implies that EHB stars, denoted by \((B - V)_{\text{EHB}}, V_{\text{EHB}}\), must satisfy

\[
(B - V)_{\text{EHB}} < (B - V) - 0.5,
\]

\[
h + 0.4 < V_{\text{EHB}} < h + 0.4 + 3.5.
\]

One small region of concern for the EHB remains undefined in the CMDs, namely, the portion just above the “left” BSS boundary with slope \(-3.5\) that also falls to the right of our vertical EHB/BSS dividing line and below the lower HB boundary. For simplicity, we treat these stars as belonging to the EHB, although note that our frequencies would not have been altered by much had we taken them to be BSSs, and even less so had we taken them to be HB stars. As such, in addition to the above criteria, EHB stars can also simultaneously satisfy

\[
(B - V)_{\text{EHB}} > (B - V) - 0.5,
\]

\[
V_{\text{EHB}} > h + 0.4,
\]

\[
V_{\text{EHB}} < -3.5(B - V)_{\text{EHB}} + (V - 2.0) + 3.5[(B - V) - 0.4].
\]

In Table 2, we give the cluster name, the number of blue straggler, HB, EHB, RGB, and core stars, and the parameters needed to make these selections: the width of the main-sequence \(w\), the position of the MSTO, and the level of the horizontal branch.

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