Higgs–inflaton coupling from reheating and the metastable Universe

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Current Higgs boson and top quark data favor metastability of our vacuum which raises questions as to why the Universe has chosen an energetically disfavored state and remained there during inflation. In this Letter, we point out that these problems can be solved by a Higgs–inflaton coupling which appears in realistic models of inflation. Since an inflaton must couple to the Standard Model particles either directly or indirectly, such a coupling is generated radiatively, even if absent at tree level. As a result, the dynamics of the Higgs field can change dramatically.

The current Higgs mass $m_h = 125.15 \pm 0.24$ GeV and the top quark mass $m_t = 173.34 \pm 0.76 \pm 0.3$ GeV indicate that in the Standard Model (SM) the Higgs quartic coupling turns negative at high energies implying metastability of the electroweak (EW) vacuum at 99% CL [1]. The (much deeper) true minimum of the scalar potential appears to be at very large field values. In the cosmological context, this poses a pressing question why the Universe has chosen an energetically disfavored state and why it remained there during inflation despite quantum fluctuations.

In this Letter, we argue that these puzzles can be resolved by a Higgs–inflaton coupling [2] which appears in realistic models of inflation. Indeed, the energy transfer from the inflaton to the SM fields necessitates interaction between the two in some form. This in turn induces a Higgs–inflaton coupling via quantum effects, even if it is absent at tree level. We find that the loop induced coupling can be sufficiently large to make a crucial impact on the Higgs field evolution.

Another factor that can affect the Higgs field dynamics is the non–minimal scalar coupling to gravity, which creates an effective mass term for the Higgs field [3, 4]. Here we assume such a coupling to be negligible. The effect of quantum fluctuations during inflation has recently been considered in [5, 6]. The conclusion is that the Hubble rate $H$ above the Higgs instability scale leads to destabilization of the EW vacuum, which poses a problem for this class of inflationary models. Related issues have been studied in [7–9].

The Higgs potential at large field values is approximated by [10]

$$V_h \simeq \frac{\lambda_h(h)}{4} h^4 ,$$

where we have assumed the unitary gauge $H^T = (0, h/\sqrt{2})$ and $\lambda_h(h)$ is a logarithmic function of the Higgs field. The current data indicate that $\lambda_h$ turns negative at around $10^{10}$ GeV [11], although the uncertainties are still significant. In the early Universe, the Higgs potential is modified by the Higgs–inflaton coupling $V_{h\phi}$ with the full scalar potential being

$$V = V_h + V_{h\phi} + V_\phi ,$$

where $V_\phi$ is the inflaton potential. Since the inflaton must couple to the SM fields either directly or through mediators as required by successful reheating, quantum corrections induce a Higgs-inflaton interaction.

In what follows, we consider a few representative examples of reheating models. We focus on the Higgs couplings to the inflaton $\phi$ which are required by renormalizability of the model. Such couplings are induced radiatively with divergent coefficients and necessitate the corresponding counterterms. The dim-4 Higgs–inflaton interaction takes the form

$$V_{h\phi} = \frac{\lambda_{h\phi}}{4} h^2 \phi^2 + \frac{\sigma_{h\phi}}{2} h^2 \phi ,$$

where $\lambda_{h\phi}$ and $\sigma_{h\phi}$ are model–dependent couplings. As we show below, the range of $\lambda_{h\phi}$ relevant to the Higgs potential stabilization is between $10^{-10}$ and $10^{-6}$ (see also [2]). For definiteness, we choose a quadratic inflaton potential [11] as a representative example of large field inflationary models,

$$V_\phi = \frac{m^2}{2} \phi^2 + \Delta V_{1\text{-loop}} ,$$

where $m \approx 10^{-5} M_{Pl}$ and $\Delta V_{1\text{-loop}}$ is the radiative correction generated by various couplings of the model. We require this correction to be sufficiently small such that the predictions for cosmological observables of the $\phi^2$–model are not affected, although some quantum effects can be beneficial [12]. The divergent contributions to $\Delta V_{1\text{-loop}}$ are renormalized in the usual fashion and the result is given by the Coleman–Weinberg potential [13].

The leading term at large $\phi$ is the quartic coupling

$$\Delta V_{1\text{-loop}} \simeq \frac{\lambda_{\phi}(\phi)}{4} \phi^4 ,$$

with $\lambda_\phi$ being logarithmically dependent on $\phi$.

The energy transfer from the inflaton to the SM fields in general proceeds both through non–perturbative effects and perturbative inflaton decay [14, 15]. In what follows, we make the simplifying assumption that the reheating is dominated by the perturbative inflaton decay such that the reheating temperature is given by

$$T_R \simeq 0.2 \sqrt{T M_{Pl}},$$

where $\Gamma$ is the inflaton decay rate.
While this assumption is essential for establishing a correlation between $\lambda_{h\phi}$ and $T_R$, it does not affect the range of $\lambda_{h\phi}$ consistent with the inflationary predictions. We consider three representative reheating scenarios which assume no tree level interaction between the Higgs and the inflaton, and compute the consequent loop–induced couplings.

1. Reheating via right–handed neutrinos. The inflaton energy is transferred to the SM sector via its decay into right–handed Majorana neutrinos $\nu_R$ which in turn produce SM matter. The added benefit of this model is that the heavy neutrinos may also be responsible for the matter–antimatter asymmetry of the Universe via leptogenesis [16]. The relevant tree level Lagrangian reads

$$-\Delta \mathcal{L} = \frac{\lambda_\nu}{2} \phi \nu_R \nu_R + y_\nu \bar{l}_L H^* \nu_R + \frac{M}{2} \nu_R \nu_R + \text{h.c.} \ ,$$

where $l_L$ is the lepton doublet, $M$ is chosen to be real and we have assumed that a single $\nu_R$ species dominates. These interactions generate a coupling between the Higgs and the inflation at 1 loop (Fig. 1). Since we are interested in the size of the radiatively induced couplings, let us impose the renormalisation condition that they vanish at a given high energy scale, say the Planck scale $M_{Pl} = 2.4 \times 10^{18}$ GeV. Then, a finite correction is induced at the scale relevant to the inflationary dynamics, which we take to be the Hubble rate $H = m\phi/\sqrt{6M_{Pl}}$, with other choices leading to similar results. We find in the leading–log approximation,

$$\lambda_{h\phi} \simeq \frac{|\lambda_\nu y_\nu|^2}{2\pi^2} \ln \frac{M_{Pl}}{H} \ ,$$

$$\sigma_{h\phi} \simeq -\frac{M |y_\nu|^2 \text{Re} \lambda_\nu}{2\pi^2} \ln \frac{M_{Pl}}{H} \ ,$$

$$\lambda_\phi \simeq \frac{|\lambda_\nu|^4}{4\pi^2} \ln \frac{M_{Pl}}{H} .$$

Here we have chosen the same renormalization condition for $\lambda_\phi$ and $\lambda_{h\phi}, \sigma_{h\phi}$. Since the dependence on the renormalization scale is only logarithmic, this assumption does not affect our results. The most important constraint on the couplings is imposed by the inflationary predictions. Requiring $\lambda_\phi \phi^4/4 \ll m^2 \phi^2/2$ in the last 60 $e$-folds of expansion (see e.g. [17]), we find $\lambda_\phi \ll 2 \times 10^{-12}$ and therefore $\lambda_\phi < 1 \times 10^{-3}$. The seesaw mechanism also limits the size of the Yukawa coupling $y_\nu$. The experimental constraints on the mass of the active neutrinos require approximately $(y_\nu v)^2/M < 1$ eV. Assuming that the perturbative decay of the inflaton dominates, the mass of the right–handed neutrinos is bounded by $M < 10^{13}$ GeV, which in turn implies $y_\nu < 0.6$. We therefore get an upper bound on the size of the Higgs–inflaton coupling,

$$\lambda_{h\phi} < 2 \times 10^{-7} .$$

Note that $\lambda_{h\phi}$ is positive and thus the inflaton creates a positive effective mass term for the Higgs. The trilinear $\phi h^2$ term is irrelevant as long as $|\lambda_\nu|\phi \gg M$, which is the case for all interesting applications. (Similarly, the cubic term $\phi^3$ is negligible.)

During the inflaton oscillation stage, the magnitude of $\phi$ decreases as $1/t$. When the effective masses of $\nu_R$ and $h$ turn sufficiently small, the decays $\phi \to \nu_R \nu_R$, $\phi \to hh$ become allowed. The constraints above imply $\Gamma(\phi \to \nu_R \nu_R) \gg \Gamma(\phi \to hh)$ and therefore the total inflaton decay width is $\Gamma = |\lambda_\nu|^2 m$, where we have neglected the $\nu_R$ mass compared to that of the inflaton. Assuming that the right–handed neutrinos decay promptly and the products thermalize (or $\nu_R$ themselves thermalize) so that $T_R \simeq 0.2\sqrt{M_{Pl}}$, we find the following correlation between the Higgs–inflaton coupling and the reheating temperature $T_R$,

$$\lambda_{h\phi} \simeq 5 \times 10^{-7} |y_\nu|^2 \left( \frac{T_R}{1.5 \times 10^{11} \text{ GeV}} \right)^2 ,$$

where $T_R$ is bounded by $1.5 \times 10^{11}$ GeV. Note that this relation holds only under the assumption of perturbative reheating. Therefore, for the neutrino Yukawa coupling and the reheating temperature within one–two orders of magnitude from their upper bounds, the dynamics of the Higgs evolution change drastically. Similar conclusions apply to models with multiple $\nu_R$ species.

2. Reheating and non–renormalizable operators. A common approach to reheating is to assume the presence of non–renormalizable operators that couple the inflaton to the SM fields. Let us consider a representative example of the following operators

$$O_1 = \frac{1}{\Lambda_1} \phi \q_L \cdot H^* t_R \ , \quad O_2 = \frac{1}{\Lambda_2} \phi \ G_{\mu\nu} G^{\mu\nu} ,$$

where $\Lambda_{1,2}$ are some scales, $G_{\mu\nu}$ is the gluon field strength and $q_L, t_R$ are the third generation quarks. These couplings allow for a direct decay of the inflaton into the SM particles. It is again clear that a Higgs–inflaton interaction is induced radiatively. In order to calculate the 1–loop couplings reliably, one needs to complete the model in the ultraviolet (UV). The simplest possibility to obtain an effective dim–5 operator is to integrate out a heavy fermion. Therefore, we introduce vector–like
FIG. 2. Leading radiatively induced scalar couplings via the vector-like quarks $Q_L, Q_R$ with the tree level interactions

$$- \Delta \mathcal{L} = y_Q \bar{q}_L H^* Q_R + \lambda_Q \phi \bar{Q}_L t_R + \mathcal{M} \bar{Q}_L Q_R + \text{h.c.},$$

where the heavy quarks have the quantum numbers of the right-handed top $t_R$. $\mathcal{M}$ is above the inflaton mass and the couplings to the third generation are assumed to dominate. One then finds that $O_1$ appears at tree level with $1/A_1 = y_Q \lambda_Q / \mathcal{M}$, whereas $O_2$ appears only at 2 loops with $1/A_2 \sim y_Q \lambda_Q y_t \alpha_s / (64\pi^2 \mathcal{M})$ and can be neglected. Using the renormalization condition that the relevant couplings vanish at the Planck scale, we get in the leading-log approximation (see Fig. 2)

$$\lambda_{h\phi} \approx \frac{3|\lambda_Q y_t|^2}{2\pi^2} \ln \frac{\mathcal{M}}{\mathcal{M}_1},$$

$$\sigma_{h\phi} \approx -\frac{3\mathcal{M} \text{Re}(\lambda_Q y_Q y_t)}{2\pi^2} \ln \frac{\mathcal{M}_1}{\mathcal{M}},$$

$$\lambda_{\phi} \approx \frac{3|\lambda_Q|^4}{2\pi^2} \ln \frac{\mathcal{M}_1}{\mathcal{M}}.$$  

where $y_t$ is the top Yukawa coupling and we have assumed $\mathcal{M} \ll \mathcal{M}_1$. Requiring smallness of the correction to the inflaton potential in the last 60 $e$-folds, we get $|\lambda_Q| < 2 \times 10^{-3}/(\ln \mathcal{M}_1/\mathcal{M})^{1/4}$ and obtain the bound

$$\lambda_{h\phi} < 10^{-7} \left( \frac{\mathcal{M}_1}{\mathcal{M}} \right)^{1/2},$$

where we have taken $y_t(\mathcal{M}) \approx 0.5$. For $\mathcal{M}$ in the allowed range, this implies $\lambda_{h\phi} < 3 \times 10^{-7}$. We find again that $\lambda_{h\phi}$ is positive and can be large enough to affect the Higgs evolution. Assuming no large hierarchy between $\lambda_Q$ and $y_Q$, we have $\phi |\lambda_Q| \gg \mathcal{M}|y_Q|$ and the trilinear $\phi h^2$ term is unimportant for the Higgs evolution.

The trilinear interaction is however important for the inflaton decay. Taking for simplicity the couplings to be real, we have $\Gamma(\phi \rightarrow th) = \lambda_Q^2 y_Q^2 m^3 / (512\pi^3 \mathcal{M}^4)$ and $\Gamma(\phi \rightarrow hh) = \sigma_{h\phi}^2 / (32\pi m)$, which implies

$$\frac{\Gamma(\phi \rightarrow th)}{\Gamma(\phi \rightarrow hh)} = \frac{\pi^2}{36y_t^2} \frac{m^4}{\mathcal{M}^4} \ll 1$$

even for $\mathcal{M}$ just above the inflaton mass. Therefore the radiatively induced coupling dominates the inflaton decay. (This conclusion can be avoided by tuning the phases of $\lambda_Q$ and $y_Q$ such that $\text{Re}(\lambda_Q y_Q) \approx 0$.)

Due to the above constraints, the reheating temperature is bounded by $T_R < 10^{-3} \mathcal{M} |y_Q| (\ln \mathcal{M}_1/\mathcal{M})^{3/4}$ for real couplings. Taking $|\lambda_Q| \mathcal{M}_1$ as the upper bound on $|y_Q| \mathcal{M}$ (see above) and allowing for the maximal value of $\mathcal{M}$ to be $10^{-2} \mathcal{M}_1$, one finds $T_R < 5 \times 10^{12}$ GeV. An approximate correlation between $\lambda_{h\phi}$ and $T_R$ can be expressed as

$$\lambda_{h\phi} \approx 10^{-1} \frac{|\lambda_Q|}{|y_Q|} \frac{T_R}{\mathcal{M}}.$$  

3. Reheating through dark matter production.

This somewhat more exotic scenario exhibits different qualitative features. It assumes that the inflaton interacts mostly with dark matter or some other SM singlet, which then produces the SM fields through rescattering. The simplest renormalizable model of this type is based on scalar DM $s$ with the tree level interactions

$$- \Delta \mathcal{L} = \lambda_{ss} \phi^2 s^2 + \sigma_{ss} s^4 + \lambda_{ss} s^2 + \frac{\lambda_s}{4} s^4 + \frac{m_s^2}{2} s^2.$$  

In this case, DM is produced both through the non-perturbative effects and inflaton decay, while the SM particles are generated via the Higgs field. Assuming that DM is much lighter than the inflaton, the induced scalar couplings in the leading-log approximation are

$$\lambda_{h\phi} \approx -\frac{\lambda_{ss} \lambda_s}{16\pi^2} \ln \frac{\mathcal{M}_1}{H},$$

$$\sigma_{h\phi} \approx -\frac{\lambda_{ss} \sigma_{ss}}{16\pi^2} \ln \frac{\mathcal{M}_1}{H},$$

$$\lambda_{\phi} \approx -\frac{\lambda_{ss}^2}{32\pi^2} \ln \frac{\mathcal{M}_1}{H}.$$  

Unlike in the previous examples, we see that $\lambda_{h\phi}$ can be of either sign. It is positive for $\lambda_{ss} \lambda_s < 0$, which is an admissible possibility. The $\phi^4$ interaction gives a small contribution to the inflaton potential for $|\lambda_{ss}| < 8 \times 10^{-6}$, which implies

$$|\lambda_{h\phi}| < 5 \times 10^{-7} |\lambda_{ss}|.$$  

Here $\lambda_{ss}$ is only restricted by perturbativity and can be as large as $O(1)$ which results in even more significant inflaton–Higgs coupling than before. The trilinear term is unimportant for the Higgs field evolution for $\lambda_{ss} \phi \gg 0$.

FIG. 3. Leading radiatively induced scalar couplings via scalar dark matter.
where the effective inflaton mass is $m$, by the inflaton mass term. The Hubble rate is dominated by the Higgs–inflaton interaction term $(2 \sqrt{m/M_{Pl}})^2$ such that the allowed range of $\lambda_{h \phi}$ is

$$10^{-10} < \lambda_{h \phi} < 10^{-6}.$$  \hfill (23)

In this range, the quantum fluctuations of $h$ during inflation are also insignificant since (i) the Higgs field is heavy and (ii) the barrier separating the two vacua is at large field values $h_{\text{bar}} \sim \sqrt{m_{h_{\phi}}/M_{Pl}} \gg H$. The lower bound on $\lambda_{h \phi}$ also guarantees that the classical evolution of $\phi$ dominates, i.e. the initial inflaton value satisfies $V_{h_{\phi}} < 5/\sqrt{m/M_{Pl}}$. The total number of $e$-folds is about $(\phi_{0}/M_{Pl})^2/4$, with $\phi_{0}$ bounded by Eq. (19).

The presence of a small trilinear term $\phi h^2$ does not affect these considerations. As long as the effective Higgs mass term remains large and positive, the Higgs field evolves to zero. In that case, its effect is negligible. The Higgs–inflaton interaction offers no solution to the cosmological problems if the effective Higgs mass term is too small or negative. In that case, $h$ is overwhelmingly likely to end up in the catastrophic true vacuum.

Since we introduce additional fields that couple to the Higgs, one may wonder how those affect the running of the Higgs quartic coupling. In the first two examples, this effect is small since the extra states are very heavy and the (negative) leading contribution to the beta–function is proportional to the fourth power of the Higgs–fermion coupling. In the case of scalar mediators, the effect can be significant depending on the scalar mass and its coupling to the Higgs. For $m_s \sim \text{TeV}$ and $\lambda_{h \phi}(H) \gtrsim 0.6$, the Higgs potential is stable up to the Planck scale (see e.g. [19]). In that case, the cosmological problems discussed in this Letter do not arise. However, for heavier $m_s$ and/or smaller couplings the electroweak vacuum is still metastable, while the stabilization mechanism described here is at work.

In summary, reheating the Universe after inflation necessitates (perhaps indirect) interaction between the inflaton and the SM fields. As a result, a Higgs–inflaton interaction is induced radiatively as required by renormalizability of the model. Such a coupling can be sufficiently large to alter drastically the Higgs field dynamics in the early Universe. In particular, it can hold the key to the question how the Universe has evolved to the energetically disfavored state, given that the current data point to metastability of the electroweak vacuum.

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