Exploration of Nonlinear Optical Properties of Triphenylamine-Dicyanovinylene Coexisting Donor-\(\pi\)-Acceptor Architecture by the Modification of \(\pi\)-Conjugated Linker

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High-tech electronic, optics, and storage devices require organic compounds with nonlinear optical (NLO) properties. This study designed D-\(\pi\)-A based dyes with donor triphenylamine (TPA) and acceptor dicyanovinylene (DCV) species by structurally modifying \(\pi\)-conjugated linkers. Our density functional theory (DFT) computations analyzed the impact of structural variations on the nonlinear optical (NLO) response of newly designed dyes. The B3LYP/6-31G(d,p) level determined the quantic chemical insights: frontier molecular orbitals (FMOs), natural bond orbitals (NBOs), and nonlinear optical (NLO) properties of the designed dyes (DPTM-1 to DPTM-12). UV-Vis analysis based on the TD-DFT/CAM-B3LYP/6-311+G(d,p) level explored the optoelectronic properties. DPTM-1 and DPTM-5 showed the highest red-shifted absorption band at 519 and 506 nm. NBO analysis shows that DPTM-1 to DPTM-12 dyes have positive values for all donors (D) and \(\pi\)-spacers but negative values for acceptors (A). The \(\pi\)-spacers act as a conveyer between donor and acceptor moieties; thus, electrons were transferred smoothly from D to A units, which resulted in a charge separation state. Our calculations show the extent of NLO response in terms of electronic transitions, polarizability \(<\alpha>\), and first hyperpolarizability \(\beta\) values. The highest value of \(\beta_{\text{total}}\) was 110,509.23 a.u. manifested in DPTM-6 due to 2,5-dimethyloxazole as a second \(\pi\)-linker, twice that of R (66,275.95 a.u.). Also, DPTM-6 and DPTM-8 exhibit the lowest energy band gap of 2.06 and 2.04 eV, respectively. In short, all DPTM-1 to DPTM-12 dyes manifested maximum absorption, lowest energy band gap, greater charge transfer from donor to the acceptor, and better first hyperpolarizability.
values as compared to the R and showed good NLO response. The present work represents new compounds with remarkable NLO properties and their applications in modern high-tech devices.

**Keywords:** nonlinear optical properties, π-conjugated linkers, density functional theory, metal-free organic dyes, triphenylamine-dicyanovinylene

**INTRODUCTION**

With the rapid rise of high-tech electronic, optics, and storage devices, organic compounds with NLO properties gained unparalleled popularity and dominance in various disciplines, such as medicine, material science, atomic, molecular, and solid-state physics, surface interface sciences, and chemical dynamics (Eaton, 1991; Peng and Yu, 1994; Tsutsumi et al., 1998; Breitung et al., 2000; Christodoulides et al., 2010). Organic NLO materials, especially with larger π-extended frames, are significantly interesting as dynamic intermolecular charge transfer (ICT) materials with excellent NLO response, facile synthesis, optical switching, frequency shifting, and better signal reception. The presence of delocalized electrons in the organic compounds leads to further enhancement in the NLO response (Anthony et al., 2008; Yamashita, 2011; Ivanov et al., 2013; Khoo, 2014). A significant amount of NLO responses has been observed in organic compounds due to π-electrons with strong electric polarization, low dielectric coefficient, quick response, and high laser damage threshold and π-bond system involves charge distribution from donor to acceptor (Sung and Hsu, 1998; Hochberg et al., 2006). Intermolecular charge transfer occurs from electron-donating to the electron-withdrawing units by the π-conjugated linkers directly linked with the first hyperpolarizability (β) (Zyss, 1987; Prasad and Williams, 1991; Drozd and Marchewka, 2005; Janjua, 2017).

HOMO and LUMO allow charge transfer, but the π-conjugated system leads to charge transfer in an electric field where the π-spacer is a basic molecule (Datta and Pal, 2005; Siddiqui et al., 2012; Garza et al., 2014). By changing the conjugation system the properties of dyes can vary and the NLO response can improve by choosing the finest length of conjugation. Appropriate arrangement of donor, acceptors, and π-bridge plays a crucial role in designing a competent organic compound (Dalton, 2001; Dalton, 2002). This appropriate arrangement enhances the electronic distribution, induces charge separation, increases absorption range towards longer wavelength, reduces charge recombination, and decreases the HOMO-LUMO energy gap, resulting in an improved NLO response. There are large dipole moments between the ground and excited state of the compounds because of ICT, including electron density transfer from D to A units through π-bridge (Haid et al., 2012; Srinivasan et al., 2017). Literature has shown that NLO response can be improved when ICT is enhanced by ring twisting and optimizing the D-A pair (Dulcic et al., 1981; Berkovic et al., 1987). The organic dyes with π-bond system involved delocalization of charge. The major effect of π-bridge on NLO activity is also important in the prediction of optimized NLO properties. Although D units have a major impact on NLO properties, one cannot ignore the role of the acceptor unit.

Different types of π-spacers are helpful in a good connection between HOMO and LUMO units to have a good NLO response (Khan et al., 2018a).

Literature is overflowing with various designs comprising A−π−D−π−A, D−A, D−π−A, D−π−A−π−D, D−A−π−A, D−π−π−A, and D−D−π−A (Khalid et al., 2020). It has been determined by both experimental and theoretical inspection that D−π−A types of designed dyes show excellent NLO responses (Khan et al., 2018b). Furthermore, the optimal length of π-conjugation, composited in between donor and acceptor, also contributes to an increased NLO response (Saeed et al., 2020). That is why, in this study, we have tailored the π-conjugated system and designed the D−π−A type of compounds (DPTM-1 to DPTM-12). To the best of our knowledge, these compounds have never been designed before for the efficient theoretical study for NLO properties.

**COMPUTATIONAL PROCEDURE**

In the present study, NBO analysis, electronic structures, absorption spectra, and NLO properties of D−π−A dyes were calculated by performing density functional theory and time-dependent density functional theory. All computational calculations were performed using Gaussian 09 package program (Olson and Boldyrev, 2012). Ground state geometry optimization of the dyes is determined in the gas phase to confirm that no imaginary frequencies are involved in dyes through the B3LYP (Civalleri et al., 2008) level of theory combined with a 6-31G(d,p) (Azm et al., 2020; Bilal Ahmed Siddique et al., 2020; Hussain et al., 2020; Mehboob et al., 2020) basis set. The HOMO-
LUMO energies and their differences were calculated using the same function. FMO investigation proved highly beneficial in understanding electronic transitions from donor to the acceptor orbital. The charge transfer interactions in the entitled compounds were observed in the NBO analysis. TD-DFT calculations with the CAM-B3LYP/6-311+G(d,p) level were used to comprehend the UV-Visible absorption spectra of the entitled molecules (Yanai et al., 2004). All input files were made by Gauss View 5.0 (Vural et al., 2017), whereas output effects were construed and visualized using Gauss View, Avogadro (Hanwell et al., 2012), and Chemcraft (Dena et al., 2019) programs. The Gaussian output presented six linear polarizability tensors ($\alpha_{xx}$, $\alpha_{yy}$, $\alpha_{zz}$, $\alpha_{xy}$, $\alpha_{xz}$, $\alpha_{yz}$) and ten first hyperpolarizability tensors ($\beta_{xxx}$, $\beta_{xyy}$, $\beta_{xzz}$, $\beta_{xyy}$, $\beta_{xzy}$, $\beta_{yzz}$, $\beta_{zzz}$, $\beta_{xxz}$, $\beta_{yyz}$, $\beta_{xyz}$) along the x, y, and z directions, respectively. Polarizabilities and first hyperpolarizability values of the design compounds (DPTM-1 to DPTM-12) have been calculated at the same level of theory. Equations 1 and 2 can be utilized for calculating the polarizability $\langle \alpha \rangle$ and first hyperpolarizability ($\beta_{total}$) of the entitled compounds (Karakas et al., 2007).

$$\langle \alpha \rangle = -\frac{1}{3} \left( \alpha_{xx} + \alpha_{yy} + \alpha_{zz} \right)$$  \hspace{1cm} (1)

$$\beta_{total} = \left[ (\beta_{xxx} + \beta_{xyy} + \beta_{xzz})^2 + (\beta_{xyy} + \beta_{xzy} + \beta_{yzz})^2 + (\beta_{zzz} + \beta_{xxz} + \beta_{xyz})^2 \right]^{1/2}$$  \hspace{1cm} (2)

RESULTS AND DISCUSSION

Khan et al. modified a D-\(\pi\)-A-based 2-((5-(2-(4-(diphenylamino) phenyl)benzo[d]thiazol-5-yl)thiophen-2-yl)methylene)malononitrile dye (R) by changing \(\pi\)-conjugated linkers between the fixed donor...
(triphenylamine) and acceptor (dicyanovinylene) species to enhance its NLO properties (Khan et al., 2018a). In this present work, eight π-linkers that were not previously reported are used to design organic dye with potential NLO responses. The molecular and optimized structures of the entitled dyes, as shown in Figures 1, 2, have three fragments, D, π-spacer, and A. In the designed compounds (DPTM-1 to DPTM-12), triphenylamine (TPA) acts as a donor and dicyanovinylene (DCV) as an acceptor unit with various π-conjugated linkers. Various combinations were made to design twelve new TPA-DCV based D-π-A compounds involving six π-spacers used as first π-linkers and two π-spacers as second π-linkers. To judge the impact of structural changes on NLO properties, eight π-linkers that were not previously reported are used to design the dyes with potential NLO responses.
properties, density functional theory (DFT) and time-dependent density functional theory (TD-DFT) calculations were performed.

**ELECTRONIC STRUCTURE**

The FMO analysis is considered a standard approach to predict the chemical stability in molecules (Gunasekaran et al., 2008). The frontier molecular orbitals, i.e., HOMO (highest occupied molecular orbital) and LUMO (lowest unoccupied molecular orbital), play an exceptional role in the absorption spectra and mechanical illustration of the compounds. Usually, HOMO is referred to as an electron donator, while LUMO is usually regarded as an acceptor (Amiri et al., 2016). Band gap (\(E_{\text{LUMO}}-E_{\text{HOMO}}\)) is considered an exceptional factor in predicting hardness, strength, softness, dynamic stability, and chemical reactivity of the deliberated dyes (Khalid et al., 2017), where a sizeable band gap shows minimum reactivity and maximum stability and hardness of a molecule. In contrast, highly reactive and soft molecules, predicted with a small \(E_{\text{LUMO}}-E_{\text{HOMO}}\) band gap, are far more polarized and serve as a finer competitor in offering the best NLO response (Parr et al., 1999; Lesar and Milišev, 2009; Chattaraj et al., 2011). \(E_{\text{HOMO}}, E_{\text{LUMO}}\) and bandgap (\(E_{\text{LUMO}}-E_{\text{HOMO}}\)) for DPTM-1 to DPTM-12 have been determined by the DFT computational analysis. The calculated values are given in Table 1.

| Compounds | \(E_{\text{HOMO}}\) | \(E_{\text{LUMO}}\) | \(\Delta E\) |
|-----------|-----------------|-----------------|-----------|
| DPTM-1    | -5.405          | -3.170          | 2.24      |
| DPTM-2    | -5.521          | -3.324          | 2.19      |
| DPTM-3    | -5.683          | -3.427          | 2.24      |
| DPTM-4    | -5.775          | -3.574          | 2.20      |
| DPTM-5    | -5.342          | -3.174          | 2.17      |
| DPTM-6    | -5.405          | -3.341          | 2.06      |
| DPTM-7    | -5.604          | -3.438          | 2.17      |
| DPTM-8    | -5.645          | -3.608          | 2.04      |
| DPTM-9    | -5.496          | -3.112          | 2.38      |
| DPTM-10   | -5.572          | -3.292          | 2.28      |
| DPTM-11   | -5.675          | -3.185          | 2.49      |
| DPTM-12   | -5.743          | -3.966          | 2.38      |

*Units in eV.*

The outcomes from the equations are represented in Table 2. The electron affinity represents electron-withdrawing ability, while electron-donating tendency can be determined by the ionization potential. Among all the entitiled dyes, maximum electron affinity is observed in DPTM-8, i.e., 3.61 a.u. while the maximum ionization potential, i.e., 5.775 a.u., is shown by DPTM-4 (Table 2). Electronegativity is a tendency to attract the electron towards itself, while chemical potential (\(\mu\)) value describes the stability of molecules. A more negative value of chemical potential represents the stability of the molecules. The highest negative value of chemical potential is determined in DPTM-11, which manifests a remarkable outcome of the used \(\pi\)-conjugated linkers. These two \(\pi\)-conjugated linkers have provided a better bridge for transferring electrons from the TPA to DCV. \(\Delta E\) of DPTM-11 was found greater than 2.49 eV. The first and second \(\pi\)-linkers 2,5-dimethylbenzo[d]oxazole and 2,5-dimethylfuran, used in DPTM-11, have interrupted the transfer of electrons from the TPA to DCV (Figures 1, 2). That is why DPTM-11 has shown the highest band gap among all the designed dyes. These smaller band gaps have shown favorable NLO properties. The HOMO-LUMO (+1, −1, +2, −2) value and band gaps are mentioned in the supplementary information (Supplementary Table 13 and Supplementary Figure 1). The structural display of HOMO-LUMO orbitals with electron density distribution pattern is shown in Figure 3. In HOMO, the orbital electron density is mainly exhibited on the donor TPA and partially present along with first \(\pi\)-linkers. In the case of LUMO, the electron density predominantly occurred on the acceptor side DCV and is slightly present along with second \(\pi\)-linkers. This revealed the charge transfer from donor to acceptor moieties and illustrated the enhanced properties of NLO materials. Structural modifications by changing the \(\pi\)-conjugated linkers exhibited remarkable results for NLO resources.

**GLOBAL REACTIVITY PARAMETERS**

The bandgap (\(E_{\text{LUMO}}-E_{\text{HOMO}}\)) is crucial in describing the global reactivity parameters such as global hardness (\(\eta\)), global softness (\(\sigma\)), global electrophilicity index (\(\omega\)), electron affinity (\(\gamma\)), ionization potential (\(IP\)) (Fukui, 1982), electronegativity (\(\chi\)), and the chemical potential (\(\mu\)) (Parr et al., 1978) and calculated by utilizing Koopmans’s theorem (Koopmans, 1934) equations.

\[
\begin{align*}
IP &= -E_{\text{HOMO}} \\
EA &= -E_{\text{LUMO}} \\
\chi &= \frac{[IP + EA]}{2} = \frac{[E_{\text{LUMO}} + E_{\text{HOMO}}]}{2} \\
\eta &= \frac{[IP - EA]}{2} = \frac{[E_{\text{LUMO}} - E_{\text{HOMO}}]}{2} \\
\mu &= \frac{E_{\text{HOMO}} + E_{\text{LUMO}}}{2} \\
\sigma &= \frac{1}{2\eta} \\
\omega &= \frac{\mu^2}{2\eta}
\end{align*}
\]

The bandgap and hardness of the molecules have a direct relation. A sizeable bandgap describes a less reactive molecule with greater hardness and high kinetic stability.
Furthermore, if a molecule has less energy bandgap, it describes the more reactive molecule, with lesser hardness and lower kinetic strength.

Among all the designed compounds, the lowest hardness value is calculated in DPTM-6, i.e., 1.032 a.u. In DPTM-7, first and second π-conjugated linkers such as 5,5′-dimethyl-2,2′-bifuran and 2,5-dimethylhexazole provided a better path for transfer of electrons from HOMO-LUMO orbital in a minimum amount of energy. The least chemical stability and the maximum hardness are observed in DPTM-11 as 1.245 a.u. The decreasing order of hardness of the investigated molecules is DPTM-11>DPTM-9>DPTM-12>DPTM-10>DPTM-3>DPTM-1>DPTM-4>DPTM-2>DPTM-5>DPTM-7>DPTM-6. Therefore, DPTM-8 has shown the lowest band gap among all the dyes, showing maximum softness and significant NLO properties.

**NATURAL BOND ORBITAL (NBO) ANALYSIS**

NBO is a technique that thoroughly explains the charge transfer and conjugative interactions between the donor and acceptor moieties (James et al., 2006; Szafran et al., 2007). It also provides a steady explanation of intermolecular interactions between two or more counterparts. It is based on the lone pair and bond pair interactions. It is a beneficial technique to study the transmission...
of electrons from the D orbital to the A orbital in the D-π-A system. The charge transfer of studied compounds findings is expressed in Table 3.

It has been observed from Table 3 that donor units contain a positive charge, due to which it has excellent electron-donating power. However, acceptor moiety holds a negative charge describing that acceptors will accept electrons effectively. The π-spacers have positive charges, demonstrating that they will not stop the electrons transfer and act as a bridge to smoothly transfer charge densities from donor to acceptor units. Transfer of charge from D (filled) orbital to A (vacant) orbital is because of the hyperconjugative and intra- and intermolecular interactions. It has been observed that the highest NBO charge values were observed for DPTM-1 and the least NBO charge values were observed for R. The most suitable push-pull architecture is seen in DPTM-1, which is conveying the charge towards π-bridge to act as a conveyer and allowed to pass the charge towards the acceptor unit. The electronic transition types of NBO (DPTM-1 to DPTM-12) are demonstrated in the supplementary information (Supplementary Tables 14–25). Thus, the results prove the successful transfer of charges from filled to vacant orbital through π-spacer. The NBO charge values of other dyes also showed a close relation to each other.

NONLINEAR OPTICAL (NLO) PROPERTIES

NLO dyes and materials are widely used in communication technology, signal processing optical switches, and memory devices. A thorough understanding of NLO properties is required for the design of these materials. Electronic properties are measured to be accountable for the power of photosensitive response, which in turn depends on linear effect (polarizability, $\alpha$) and nonlinear effect (hyperpolarizabilities, $\beta$ and $\gamma$, etc.).

Therefore, unfolding of NLO response of (DPTM-1 to DPTM-12), the nonlinear and linear factors are estimated using (B3LYP) level with 6-31G (d, p) basis set. The $\langle \alpha \rangle$ values in Table 4 describe the effect of π-linkers on NLO and linear properties of
entitled compounds. Polarizability is defined by a second rank tensor $\langle \alpha \rangle$. The $\langle \alpha \rangle$ of the $\text{R}$ observed is 645.71 a.u. (Khan et al., 2018a). Odd number of design compounds having 2,5-dimethylfuran as a second $\pi$-linker, the highest value of $\langle \alpha \rangle$ is observed for DPTM-5 (677.51 a.u.) with 5,5′-dimethyl-2,2′-bifuran as a conjugated first $\pi$-linker. This value lessens to 663.48 a.u. in DPTM-1 containing 5-dimethylfuran[3,2-b]furan as a first $\pi$-linker; this value more decreases to 640.19 a.u. in DPTM-3 having 2,5-dimethylxazo[5,4-d]oxazole as a first $\pi$-linker. In case of DPTM-7, DPTM-9, and DPTM-11 the value of $\langle \alpha \rangle$ further decreases to 625.88, 619.24, and 595.48 a.u. with 2,2′-dimethyl-5,5′-bioxazole, 2,5-dimethylbenzofuran, and 2,5-dimethylbenzo[d]oxazole first $\pi$-linker, respectively. In the same way, DPTM-2, DPTM-4, DPTM-6, DPTM-8, DPTM-10, and DPTM-12 have 2,5-dimethylxazo as a second $\pi$-linker. Among these compounds, DPTM-6 comprises the highest value of $\langle \alpha \rangle$ (668.19 a.u.) with 5,5′-dimethyl-2,2′-bifuran as a first $\pi$-linker. Moreover, this value decreases to 649.34, 629.01, 619.24, and 605.58 a.u. for DPTM-2, DPTM-4, DPTM-8, and DPTM-10 comprising 2,5dimethylfuran[3,2-b]furan, 2,5-dimethylxazo[5,4-d]oxazole, 2,2′-dimethyl-5,5′-bioxazole, and DPTM-2,5-dimethylbenzofuran as first $\pi$-linker, respectively. The least value of $\langle \alpha \rangle$ is observed in case of DPTM-12 (584.13 a.u.) with 2,5-dimethylbenzo[d]oxazole as a first $\pi$-linker. DPTM-5 showed an amplified value of $\langle \alpha \rangle > 677.51$ (a.u.), indicating a strong NLO effect, while DPTM-12 molecule reveals retracted value of $\langle \alpha \rangle > 584.13$ a.u. The overall decreasing order of polarizability is DPTM-5 $>$ DPTM-6 $>$ DPTM-1-R $>$ DPTM-3 $>$ DPTM-4 $>$ DPTM-7 $>$ DPTM-8 $>$ DPTM-9 $>$ DPTM-10 $>$ DPTM-11 $>$ DPTM-12 (Table 4).

According to the literature, polarizability of a molecule is influenced by the energy bandgap between LUMO and HOMO. Small amounts of energy gap are required to demonstrate a high level of linear polarizability. Generally speaking, compounds with a small $\Delta E$ and large $\langle \alpha \rangle$ value suggest high $\beta$ values (Qin and Clark, 2007). Electronic transitions along the $x$ and $y$ axes are commonly used to calculate polarizability. To illustrate dipole polarizability, Eq. 10 is utilized:

$$\alpha \propto \left(\frac{M_{xx}^2}{E_{g_{\text{wm}}}}\right)$$

The transition moment is indicated as $M_{xx}$ and transition energy between HOMO and LUMO is indicated as $E_{g_{\text{wm}}}$. This equation shows that $\alpha$ is directly related to the square of transition moment.
and has an inverse relation with \( E_{gm} \). It is intimated that a molecule with a higher \( M_{KM}^g \) and lower \( E_{gm} \) value possesses the maximum value of \( \alpha \), so it contains amplified hyperpolarizability value. Thus, in order to estimate desirable NLO properties of moieties, dipole polarizabilities are contemplated as computable value. Thus, in order to estimate desirable NLO properties of moieties, dipole polarizabilities are contemplated as computable measurements. NLO response of dyes with regard to the first-order hyperpolarizability is described in Table 5. The remaining first-order hyperpolarizability tensors are exhibited in the supplementary information (Supplementary Table 26).

A third rank tensor represents the first hyperpolarizability. The \( \beta_{total} \) of the \( R \) observed is 66,275.95 a.u. (Khan et al., 2018a). Among all the compounds having 2,5-dimethylfuran as a second \( \pi \)-linker \( \text{DPTM-3} \) has the highest value of \( \beta_{total} (93,827.84 \text{ a.u.}) \) with 2,5-dimethoxazolo[5,4-d]oxazole as first \( \pi \)-linker. This value then decreases to 92,976.03 a.u. in \( \text{DPTM-5} \) that further diminishes to 85,798 a.u. in \( \text{DPTM-1} \). A decrease in the \( \beta_{total} \) occurs from \( \text{DPTM-7} \) to \( \text{DPTM-9} \) and \( \text{DPTM-11} \), with 83,266.12, 59,359.72, and 49,099.29 a.u. Similarly in the compounds having 2,5-dimethoxazolo as a second \( \pi \)-linker, \( \text{DPTM-6} \) is observed with the highest value of \( \beta_{total} (110,509.23 \text{ a.u.}) \) and the least value is observed in \( \text{DPTM-12} \) (58,930.08 a.u.). The overall increasing order for \( \beta_{total} \) of all

TABLE 6 | Transition energy (eV), maximum absorption wavelengths \((\lambda_{max})\), oscillator strengths \((f_{os})\), light-harvesting efficiency \((LHE)\), transition moment \((M_{KM}^g \text{ a.u.})\), and major molecular orbital transitions of the designed compounds.

| Compounds | \( E \) (eV) | \( \lambda_{max}(\text{nm}) \) | \( f_{os} \) | LHE | \( \mu_{gm}(\text{a.u.}) \) | Major MO transitions |
|-----------|-------------|-----------------|--------|-----|-----------------|---------------------|
| DPTM-1    | 2.386       | 519.57          | 2.143  | 0.992 | 5.63            | H-1L(20%), HL(71%)  |
| DPTM-2    | 2.480       | 500.03          | 2.125  | 0.992 | 5.96            | H-1L(26%), HL(82%)  |
| DPTM-3    | 2.525       | 491.06          | 2.197  | 0.993 | 7.05            | H-1L(27%), HL(65%)  |
| DPTM-4    | 2.580       | 480.50          | 2.186  | 0.993 | 6.79            | H-1L(24%), HL(61%)  |
| DPTM-5    | 2.449       | 506.34          | 1.984  | 0.989 | 5.96            | H-1L(28%), HL(60%)  |
| DPTM-6    | 2.524       | 491.26          | 1.921  | 0.988 | 7.05            | H-1L(27%), HL(65%)  |
| DPTM-7    | 2.737       | 452.99          | 1.966  | 0.989 | 6.09            | H-1L(43%), HL(40%)  |
| DPTM-8    | 2.785       | 445.12          | 1.880  | 0.986 | 6.89            | H-1L(35%), HL(43%)  |
| DPTM-9    | 2.690       | 480.92          | 1.743  | 0.981 | 4.96            | H-1L(35%), HL(54%)  |
| DPTM-10   | 2.795       | 443.62          | 1.747  | 0.982 | 6.65            | H-1L(29%), HL(53%)  |
| DPTM-11   | 2.814       | 440.55          | 1.822  | 0.984 | 4.03            | H-1L(48%), HL(42%)  |
| DPTM-12   | 2.960       | 420.34          | 1.888  | 0.987 | 5.56            | H-1L(42%), HL(41%)  |

The optical efficiency is directly related to a factor named light-harvesting efficiency (LHE). A larger LHE value is linked to the higher photocurrent response of the compound and vice versa. Eq. 11 used to represent LHE is (Nalwa, 2000)
LHE = 1 − 10^−4 \quad (11)

In Eq. 11, f stands for strength of oscillations. LHE of DPTM-3 and DPTM-4 is the highest among all the investigated compounds as given in Table 6. These calculations indicate a better connection between donor and acceptor units leading to a potential NLO response. Oudar and Chemla (Oudar and Chemla, 1977) presented the two-level models which explain the relationship between charge transfer transitions, and the first hyperpolarizability depends upon sum-over-states (SOS) relation showed in

\[ \beta_{\text{CT}} = \frac{\Delta \mu_{\text{gm}} f_{\text{gm}}}{E^3_{\text{gm}}} \quad (12) \]

In this expression, \( \beta_{\text{CT}} \) is the first hyperpolarizability, \( \Delta \mu_{\text{gm}} \) represents dipole moment difference, \( f_{\text{gm}} \) represents the strength of oscillation from the lower to higher state, and \( E^3_{\text{gm}} \) represents the cube of transition energy. The product of \( f \Delta \mu_{\text{gm}} \) and \( f_{\text{gm}} \) is directly related to the first hyperpolarizability, while transition energy \( E^3_{\text{gm}} \) and first hyperpolarizability (\( \beta \)) value have an inverse relation. So, NLO material with a higher \( \Delta \mu_{\text{gm}} \) \( f_{\text{gm}} \) value, and charge transfer of lower energy have an excellent NLO response with a large \( \beta \) value. The relation between the \( \beta_{\text{total}} \) and the constant \( \beta_{\text{CT}} \) of investigated compounds is manifested in Figure 5. It is evident from Figure 5 that \( \beta_{\text{tot}} \) values are in good contract with the formula (\( \Delta \mu_{\text{gm}} f_{\text{gm}} / E^3_{\text{gm}} \)) values recommended by the two-level model. These conclusions indicate that using various \( \pi \)-bridges is an important methodology for designing new appealing D-\( \pi \)-A structures with excellent NLO properties. This leads to NLO materials with an effective photoelectric and optical response.

CONCLUSION

In summary, the objective of the present study was to investigate NLO properties of metal-free, theoretically designed organic dyes (DPTM-1 to DPTM-12) comprising of various \( \pi \)-linkers mixed with D and A. To elucidate the impact of various \( \pi \)-bridges on NLO properties, TDDFT and DFT methods have been employed on designed dyes (DPTM-1 to DPTM-12). Electronic structures, absorption spectra, energy difference, and first hyperpolarizability values are explained by the quantum chemical methods. All dyes have shown maximum absorbance in the visible region, low transition energy, LHE, and oscillating strength values as compared to R. The highest red-shifted absorption spectra have been observed at 519.57 nm in DPTM-1. The NBO analysis explained the charge transfer mechanism from donor to acceptor part through the \( \pi \)-conjugated linkers. The highest NBO charge transfer was observed for DPTM-1. The FMO analysis illustrated electron density of all dyes, in HOMO electron density is primarily located on the DPA and first \( \pi \) linkers and in LUMO electron density is located at the DCV. Electron density transfer from the HOMO orbital to LUMO orbital plays an important role to enhance the NLO properties. The lowest HOMO to LUMO energy difference was observed for DPTM-4, DPTM-6, and DPTM-8 with the lowest \( E_{\text{gap}} \) of 2.20, 2.06, and 2.04 eV, respectively. The greater amount of NLO properties was 101,482.89, 110,509.23, and 99,698.28 a.u. in DPTM-4, DPTM-6, and DPTM-8, respectively, with urea as a standard. The DPTM-6 \( \beta_{\text{tot}} \) value is twenty-six hundred times greater than urea. Among all designed compounds these compounds exhibit lowest energy band gap and highest NLO response. This present work also depicted the importance of structural tailoring of \( \pi \)-linkers in D-\( \pi \)-A dyes. It is a valuable theoretical approach for the researchers to design...
new excellent NLO materials. This work also provided new ways to experimentally synthesize new appealing NLO materials for their use in optics and electronics devices.

DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/Supplementary Material; further inquiries can be directed to the corresponding authors.

AUTHOR CONTRIBUTIONS

All authors listed have made a substantial, direct, and intellectual contribution to the work and approved it for publication.

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SUPPLEMENTARY MATERIAL

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