A More General MSSM Parameter Scan

Here a more general MSSM parameter scan than that described in section 8.3 is considered, following [1,2]. In addition, while the benchmark results given there used the Renormalisation Group Equation (RGE) approach [3] with recent modifications bringing them into agreement with the Full Diagrammatic Calculations (FDC) [4], here the FDC are used directly.

The parameters shown in Table 1 are the input parameters for the calculations of the physical Higgs, sfermion, chargino, and neutralino masses and production rates, and they are varied in the ranges shown. The A mass is scanned in steps of 1 GeV/c^2 up to 200 GeV/c^2 and in larger steps thereafter. For each m_A, 2700 parameter combinations are investigated. The range of tan β is restricted to 0.5 ≤ tan β ≤ 50: the lower bound is described for example in [6], and affects the theoretically allowed regions in the (m_h,m_A) plane; varying the upper bound has no significant effect on the results. The range of µ is restricted to ±500 GeV/c^2, since very large values are disfavored by Charge- and Color-Breaking (CCB) global minima in the MSSM [5]. Finally, in the RGE approach used for the benchmark scan, \( X_t = \sqrt{6} M_S \) defined the so-called \( m_{h}^{max} \) scenario, and \( X_t = 0 \) the no mixing scenario. In the FDC used here, the maximum scalar Higgs mass is obtained for \( A = 2M_S \), where \( X_t^{FDC} = A - \mu / \tan \beta \). Compared to previous similar studies [1,2], the range of A is extended from ±1M_S to ±2M_S in order to include the maximal Higgs boson mass in the scan. The top quark mass is fixed at \( m_t = 175 \) GeV/c^2. A value of \( m_t = 180 \) GeV/c^2 would increase the calculated \( m_h \) values by 2 GeV/c^2 for large tan β and by 4 GeV/c^2 for small tan β.

| Parameter | \( m_A \) | tan β | \( M_S \) | \( M_2 \) | µ | A or \( X_t \) |
|-----------|--------|------|--------|--------|---|---------|
| this scan | 20 — 1000 | 0.5 — 50 | 200 — 1000 | 200 — 1000 | −500 — +500 | −2M_S — +2M_S |
| benchmark | 20 — 1000 | 0.5 — 50 | 1000 | 200 | −200 | 0, \( \sqrt{6} M_S \) |

Table 1: Ranges of SUSY parameters at the electroweak scale used for independent variation in the more general MSSM parameter scan compared with those used in the benchmark scan of section 8.3. All masses are given in GeV/c^2.

For some parameter combinations the branching ratio into a pair of neutralinos is dominant. In such a case no limit can be derived using the channels studied in this paper. Therefore, limits from the DELPHI search for invisible decays of neutral Higgs bosons [12] are also used.

The following constraints have also been considered:

- The rate of the flavour changing neutral current process \( b \to s\gamma \) [7]. In the SM only amplitudes with virtual W± exchange contribute, while in the MSSM there are additional contributions from supersymmetric particles and Higgs bosons [8].
- The electroweak parameter \( \Delta \rho = \alpha_m T_{MSSM} [9] \). The MSSM contributions are constrained by experiment: \( T_{MSSM} < 0.08 [10] \).
- Chargino and neutralino mass limits from direct searches [11].

But these constraints have little influence on the excluded parameter regions with the present Higgs mass limits. Therefore, the excluded parameter sets are determined from the Higgs boson searches alone.

Figures 1 to 3 present the results in the \((m_h,m_A)\), \((m_h,\tan \beta)\), and \((m_A,\tan \beta)\) planes respectively. A given \((m_h,m_A)\) combination, for example, is excluded if all contributing

\footnote{These calculations changed the expected \( b \to s\gamma \) rates significantly. However, not all contributing terms are included and resulting assumptions are not valid in this more general scan.}
SUSY parameter sets in the ranges defined in Table 1 are excluded at more than 95% confidence level after combining all search channels using the likelihood ratio method \[13\]. The figures show three regions:

- the 95% CL excluded region (light grey),
- the theoretically not allowed region (dark).
- the allowed region (white),

and Fig. \[1\] also shows the region excluded by the benchmark scan (dotted line): the region excluded by the more general scan is smaller. In particular, the benchmark limits of 82.6 GeV/c\(^2\) on the h mass and 84.1 GeV/c\(^2\) on the A mass are reduced to 75 GeV/c\(^2\) and 78 GeV/c\(^2\), respectively. Comparison of the FDC cross sections used here and the RGE calculations used for the benchmark scan confirms that this is due to the reduced production cross-sections allowed by the extended parameter range, not due to differences between the FDC and RGE calculations. As illustrated in Table 2, low unexcluded \(m_h\) values are typically obtained for large mixing in the stop sector (large \(A\), large \(|\mu|\)).

In conclusion, the scan over a larger parameter region reduces the mass limits given in sections 8.3 and 9 by 8 GeV/c\(^2\) for the scalar and by 6 GeV/c\(^2\) for the pseudoscalar Higgs boson.

### Table 2: Examples of unexcluded parameter combinations in the more general MSSM scan.

Cross-sections for Higgs boson bremsstrahlung and pair-production are given for \(\sqrt{s} = 189\) GeV. All masses are given in GeV/c\(^2\) and cross-sections in pb.

| \(m_3\) | \(m_h\) | \(\tan\beta\) | \(M_S\) | \(M_2\) | \(\mu\) | \(A/M_2\) | \(X_i^{FD}\) | \(m_{\tilde{t}_1}\) | \(m_{\tilde{t}_2}\) | \(\sigma^{189}_{hZ}\) | \(\sigma^{189}_{hA}\) |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 80 | 78 | 8 | 1000 | 200 | 500 | 2 | 1938 | 979 | 1048 | 0.07 | 0.09 |
| 85 | 80 | 12 | 200 | 1000 | -500 | 1 | 242 | 162 | 333 | 0.00 | 0.06 |
| 85 | 86 | 10 | 1000 | 1000 | 500 | 2 | 1950 | 824 | 1174 | 0.03 | 0.04 |
| 90 | 86 | 4.4 | 1000 | 200 | -100 | -2 | -1977 | 824 | 1174 | 0.11 | 0.02 |

Table 2: Examples of unexcluded parameter combinations in the more general MSSM scan. Cross-sections for Higgs boson bremsstrahlung and pair-production are given for \(\sqrt{s} = 189\) GeV. All masses are given in GeV/c\(^2\) and cross-sections in pb.

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Figure 1: MSSM exclusion based on all DELPHI data from $\sqrt{s} = 161$ GeV to 189 GeV in the framework of the more general parameter scan. The region excluded at 95% CL (light grey), the unexcluded region (white) and the theoretically forbidden region (dark grey) are shown. The dotted line marks the allowed region obtained with the benchmark scan under the assumption of maximal mixing in the stop sector.
Figure 2: MSSM exclusion based on all DELPHI data from $\sqrt{s} = 161$ GeV to 189 GeV in the framework of the more general parameter scan. The region excluded at 95% CL (light grey), the unexcluded region (white) and the theoretically forbidden region (dark grey) are shown.
Figure 3: MSSM exclusion based on all DELPHI data from $\sqrt{s} = 161$ GeV to 189 GeV in the framework of the more general parameter scan. The region excluded at 95% CL (light grey) and the unexcluded region (white) are shown.