Parameterizing radiative transfer to convert MAX-DOAS dSCDs into near-surface box-averaged mixing ratios

R. Sinreich\textsuperscript{1}, A. Merten\textsuperscript{2,*}, L. Molina\textsuperscript{3}, and R. Volkamer\textsuperscript{1,4}
\textsuperscript{1}Department of Chemistry and Biochemistry, University of Colorado at Boulder, Colorado, USA
\textsuperscript{2}Institute for Environmental Physics, University of Heidelberg, Heidelberg, Germany
\textsuperscript{3}Molina Center for Energy and the Environment, La Jolla, CA, USA
\textsuperscript{4}Cooperative Institute for Research in the Environmental Studies, Boulder, Colorado, USA
*now at: Fraunhofer-Institut für Photonische Mikrosysteme, Dresden, Germany

Correspondence to: R. Volkamer (rainer.volkamer@colorado.edu)

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Abstract. We present a novel parameterization method to convert multi-axis differential optical absorption spectroscopy (MAX-DOAS) differential slant column densities (dSCDs) into near-surface box-averaged volume mixing ratios. The approach is applicable inside the planetary boundary layer under conditions with significant aerosol load, and builds on the increased sensitivity of MAX-DOAS near the instrument altitude. It parameterizes radiative transfer model calculations and significantly reduces the computational effort, while retrieving \(\sim 1\) degree of freedom. The biggest benefit of this method is that the retrieval of an aerosol profile, which usually is necessary for deriving a trace gas concentration from MAX-DOAS dSCDs, is not needed.

The method is applied to NO\textsubscript{2} MAX-DOAS dSCDs recorded during the Mexico City Metropolitan Area 2006 (MCMA-2006) measurement campaign. The retrieved volume mixing ratios of two elevation angles (1\textdegree{} and 3\textdegree{}) are compared to volume mixing ratios measured by two long-path (LP)-DOAS instruments located at the same site. Measurements are found to agree well during times when vertical mixing is expected to be strong. However, inhomogeneities in the air mass above Mexico City can be detected by exploiting the different horizontal and vertical dimensions probed by the MAX-DOAS and LP-DOAS instruments. In particular, a vertical gradient in NO\textsubscript{2} close to the ground can be observed in the afternoon, and is attributed to reduced mixing coupled with near-surface emission inside street canyons. The existence of a vertical gradient in the lower 250 m during parts of the day shows the general challenge of sampling the boundary layer in a representative way, and emphasizes the need of vertically resolved measurements.

1 Introduction

There are different ways to measure trace gases in the atmosphere. In situ techniques detect very localized trace gas information, and are able to resolve concentration gradients in plumes as air masses move across the instrument inlet. Such measurements face a challenge, which consists in how to assess representative concentrations over extended spatial scales as they are being predicted by atmospheric models and measured by satellites. In contrast, multi-axis differential optical absorption spectroscopy (MAX-DOAS) measurements integrate over a long distance and measure trace gases through the whole atmosphere (Hönninger and Platt, 2002), which inherently averages trace gas inhomogeneities. MAX-DOAS is an application of the well-established DOAS technique. DOAS uses the wavelength position and optical density of narrow band absorption features (< 5 nm width) to selectively detect and quantify trace gases by applying Lambert–Beer law (Platt, 1994; Platt and Stutz, 2008). In particular, MAX-DOAS uses scattered sunlight observed from multiple viewing directions, which increases the sensitivity to trace gases close to the surface due to differences in the respective light-path distributions; this means that, in

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general, a lower “elevation angle” leads to longer light paths through a trace gas layer near the instrument altitude and thus to a stronger absorption signal (elevation angle is defined as the angle between the horizontal and the pointing direction of the telescope) (e.g., Hönninger and Platt, 2002; van Roozendael et al., 2003; Hönninger et al., 2004; Wagner et al., 2004). However, the presence of aerosols in the troposphere can shorten (or lengthen) these light paths. The primary quantity of DOAS measurements is the differential slant column density (dSCD), which is the difference between integrated concentrations along the averaged light path of a measurement with low elevation angle and one of a reference (typically from the zenith). The light-path distribution (different photon paths from the sun through the atmosphere to the collecting telescope) of MAX-DOAS measurements is initially not known, and can be simulated with radiative transfer models. Since the dSCD value depends on the light path through the absorber layer, the knowledge of the aerosol profile, in general, is a prerequisite for the retrieval of a trace gas concentration from MAX-DOAS measurements. In contrast, long-path DOAS (LP-DOAS) uses an artificial light source whose light is commonly retro-reflected at a distance (typically up to 15 km) and collected with a telescope at the place of the light source. Thus, for LP-DOAS the light path is given by twice the distance of telescope/light source and retro-reflector and therefore well defined. The LP-DOAS light beam is usually close to the surface (ca. 1–100 m average height) (e.g., Wang et al., 2006) and cannot be used to derive information from higher altitudes. It is still sensitive to local emissions; however, horizontal concentration gradients are inherently averaged over the light beam distance. While in theory, LP-DOAS can realize longer light paths close to the surface than MAX-DOAS (Platt and Stutz, 2008), limitations exist in the available line of sights due to the need to find appropriate places for the setup of retro-reflectors.

The conversion of MAX-DOAS dSCDs into concentrations or volume mixing ratios (VMRs) can be a challenge since the photon light paths through the atmosphere from the sun to the MAX-DOAS device are unknown. The easiest approach is the geometric approximation introduced by Hönninger and Platt (2002). However, it does not account for aerosols in the atmosphere, which can significantly influence the light paths. Approaches which consider aerosols are two-step techniques and use radiative transfer modeling (RTM), which simulates photon light paths through the atmosphere. First, the aerosol profile is derived which, then in a second step, is used to determine the trace gas profile. This has been done using optimal estimation (Rodgers, 2000; applied by, e.g., Irie et al., 2008; Inomata et al., 2008; Clemer et al., 2010), which needs a priori assumptions and can use several wavelengths for enhancing the information content of the measurement. A similar method is the regularization (Steck, 2002; applied by Prados-Roman et al., 2011). However, both methods need relatively high computational effort. Trace gas profile retrievals have also been performed by manual iteration until the RTM results match the measurement (e.g., Heckel et al., 2005). Simpler methods make certain presumptions about the profile (e.g., the height or shape of a profile), and focus on a few key parameters (e.g., Wittrock et al., 2004; Sinreich et al., 2005; Wagner et al., 2011), which gives coarser profiles but relatively good VMR/concentration results. Here we present a new method to convert MAX-DOAS dSCDs into near-surface box-averaged VMRs in the lowest layer(s) of the planetary boundary layer (PBL). It is a one-step method and is applicable in cases when aerosols constrain the light path in a trace gas layer. The differential light path (path difference between low elevation angle and a reference with a high elevation angle) is determined, which is used to derive the trace gas VMR. Although, with this method, radiative transfer calculations are performed, the computational effort is less compared to optimal estimation profile calculations or regularization. The derived near-surface box VMRs can serve as anchors for the a priori estimates in the lowest layer of more-complex profile retrievals in order to increase computational efficiency (however, it does not provide independent information).

In the following Sect. 2 the parameterization method is described. In Sect. 3, it is applied to MAX-DOAS dSCD measurements of NO₂ during the Mexico City Metropolitan Area 2006 (MCMA-2006) measurement campaign. The thus-derived VMRs obtained from MAX-DOAS measurements pointing in three different directions are compared with LP-DOAS measurements (Merten, 2008) in two (nearly opposite) horizontal directions at roof-top level.

2 Description of the parameterization method

MAX-DOAS performed from the ground uses the general rule that the lower the elevation angle, the higher the absorption signal for a trace gas layer located close to ground. However, the presence of an elevated aerosol load in the lowest atmospheric layer shortens the light paths. This can happen to the extent that the light-path lengths of the lowest elevation angles do not differ significantly from that of a nearby elevation angle. This incidence can be used to derive near-surface box-averaged VMRs as shown in this paper, which often happens in a polluted environment or even in the marine boundary layer.

In a simplified way, Fig. 1 illustrates a scenario of an absorber layer (light blue) located in the PBL with a significant aerosol load close to the ground. On the right-hand side, the corresponding height concentration profile of the absorber is plotted in pink. Sunlight (yellow arrows) is reaching the atmosphere under a solar zenith angle θ and is scattered (indicated by red dots) considering a simplified single-scattering case (but the concept is also valid for multi-scattering cases). In the atmosphere, the sunlight is scattered either above or inside an absorber layer located in the PBL close to the ground,
The effective height of the scattering events (in the two absorption signals (covering the distance from the sun in time to the measurement spectrum). Thus, the corresponding absorption signals (covering the distance from the sun to the effective height of the scattering events) in the two spectra mainly cancel out applying the DOAS method, resulting in differential effective path lengths ($dL_{\text{eff}}$). Then, the box-averaged concentration $\tilde{c}$ relates to the dSCD as follows, which, in general, is valid also for an inhomogeneous vertical profile (see also Fig. 2):

$$\text{dSCD} = \sum_i \tilde{c}_i \cdot dL_i = \tilde{c} \cdot dL_{\text{eff}}, \quad (1)$$

with dSCD as the dSCD for the absorber, $\tilde{c}_i$ as the mean concentration of the absorber along the differential path with the length $dL_i$ on which photon $i$ travels.

In order to be able to quantify $dL_{\text{eff}}$, the light-path distribution of a measurement must be derived. A tracer for the light-path distribution can be found in the absorption of the trace gas $O_4$ (e.g., Wagner et al., 2004; Sinreich et al., 2005; Frieß et al., 2006). The concentration of the oxygen dimer $O_4$ is proportional to the concentration of $O_2$ squared (Greenblatt et al., 1990; Volkamer, 1996). Thus, the concentration profile shape is well known and is quantitatively dependent only on the air density. Changes in the dSCDs of $O_4$ indicate changes in the state of the atmosphere (i.e., mainly aerosol load) and measurement geometry (i.e., elevation angle, relative azimuth angle to the sun and solar zenith angle), respectively.

In cases in which the $O_4$ dSCDs of the lowest elevation angles are the same (referred to as collapsing of the dSCDs in the further text) the $O_4$ dSCD can be used to determine the effective light-path length in the PBL to the telescope. This path length then allows the calculation of the near-surface box-averaged VMR of the trace gas of interest according to Eq. (1). As illustrated in Fig. 2 with NO$_2$ as example for the trace gas of interest, the dSCDs (of a low elevation angle) of $O_4$ and NO$_2$ are the inputs from the measurement (left-hand side). The collapsing of the $O_4$ dSCDs of the lowest elevations angles to a single value within the analysis error is a prerequisite for applying this method since this ensures that the scattering events happened at comparable distances. Then the collapsing of the NO$_2$ dSCDs ensures that the (last) scattering events happened in the NO$_2$ layer and that the NO$_2$ layer can be approximated close enough to a homogeneous near-surface layer (yielding an average box profile concentration or VMR value). Thus, when applying it to measurement data, appropriate filtering is performed before further processing the data. If a non-box profile is assumed for the trace gas (NO$_2$), the collapsing of the trace gas is not a necessary condition, but in this case the trace gas profile shape must be known (see Supplement for a linearly decreasing profile shape). By dividing the filtered $O_4$ dSCD by the typical $O_4$ concentration at instrument altitude ($c_{O_4,\text{instr}}$), a differential $O_4$ equivalent path length $L_{eq,O_4}$ is calculated:

$$L_{eq,O_4} = \frac{\text{dSCD}_{O_4}}{c_{O_4,\text{instr}}}. \quad (2)$$

Here it is assumed that the $O_4$ concentration does not change significantly between the altitude of the instrument and the
effective scattering event. The differential O₂ equivalent path length is the light-path length from the effective scattering event to the telescope if O₂ and the trace gas (NO₂) had the same concentration profile shape (here a box profile), which typically is not the case. In a next step, radiative transfer modeling is performed in order to calculate a correction factor that accounts for the different vertical profile shapes of the exponentially decreasing O₄ concentrations with height and the homogenous layer for NO₂ (Volkamer et al., 2009). In addition, the correction factor can account for different absorbing wavelengths of the two gases. Multiplication of the differential O₂ equivalent path length with the correction factor yields the differential effective path length. Dividing the NO₂ dSCD by the differential NO₂ effective path length leads to the average NO₂ concentration or VMR in a box that reaches from the ground to height hₐ:

$$h_{\text{eff}} = d_{\text{eff}} \cdot \sin \alpha,$$

with α as the elevation angle.

The correction factor $f_c$ is calculated as the ratio of the trace gas (NO₂) concentration that is retrieved by radiative transfer calculations if $L_{\text{eq}, \text{O}_4}$ is used as path length ($c_{\text{retrieved}}$) and the trace gas concentration that is input for the radiative calculations ($c_{\text{real}}$), which is considered to be the real concentration:

$$f_c = \frac{c_{\text{retrieved}}}{c_{\text{real}}} = \frac{\text{dSCD}_{\text{NO}_2}}{L_{\text{eq}, \text{O}_4}} \cdot \frac{\text{VCD}_{\text{O}_4}}{\text{VCD}_{\text{NO}_2}} \cdot \frac{\text{PBLh}}{\text{PBLh}},$$

where dSCD_{NO₂} is the retrieved NO₂ dSCD calculated from a radiative transfer model for a specific solar zenith angle, elevation angle, wavelength, NO₂ vertical profile etc., and VCD_{NO₂} and PBLh are the NO₂ vertical column density (VCD) and the PBL height.

The differential air mass factor (dAMF) is defined as the ratio of the differential slant (dSCD) and vertical column density (VCD), where the latter one is the integrated concentration over the height. The AMF is a measure for the light-path enhancement compared to the vertical path through the atmosphere. Together with Eq. (2) follows

$$f_c = \frac{\text{dAMF}_{\text{NO}_2} \cdot \text{PBLh} \cdot c_{\text{O}_4\text{inst}}}{\text{dAMF}_{\text{O}_4} \cdot \text{VCD}_{\text{O}_4}},$$

where dAMF_{NO₂} and dAMF_{O₄} are the dAMFs for NO₂ and O₄, and VCD_{O₄} is a typical O₄ VCD for the measurement site.

The box-averaged near-surface volume mixing ratios VMR_{NO₂} can then be calculated applying the following equation:

$$\text{VMR}_{\text{NO}_2} = \frac{1}{f_c} \cdot \frac{\text{dSCD}_{\text{NO}_2} \cdot c_{\text{O}_4\text{inst}}}{\text{dSCD}_{\text{O}_4}} \cdot \frac{1}{\text{CF}},$$

with dSCD_{NO₂} and dSCD_{O₄} as measured SCDs for NO₂ and O₄, and CF as the conversion factor from the concentration to the VMR.

In this paper we used the radiative transfer model McArtim (Deutschmann, 2009; Deutschmann et al., 2011) for the calculation of the correction factors. Also, the modeled dSCDs (or dAMFs) underlying the correction factors are calculated by the SCD of a given elevation angle minus the reference SCD (zenith direction) at the same solar zenith angle (SZA).

The correction factor is not a constant. In general, it depends on any factor of the state of the atmosphere (aerosol optical density, PBL height, etc.) and on the measurement geometry (solar zenith angle, elevation angle, etc.). However, the correction factors of the different elevation angles show a typical dependence towards the AOD. In order to illustrate this dependence, Fig. 3 shows calculated correction factors as a function of aerosol optical density (AOD) for different elevation angles with an arbitrarily picked scenario as example (477 nm, 30° SZA and 1 km PBL height). For the underlying radiative transfer calculations, the trace gas profile has been chosen as a box profile with a constant mixing ratio in the PBL. The aerosol profile also has constant aerosol extinction up to the PBL height (in this paper, the trace gas layer height and the aerosol layer height are assumed to be the same unless it is stated otherwise). The trace gas is chosen to be a weak absorber, which absorbs at the O₄ wavelength of 477 nm. The elevation angles are 1°, 3°, 6°, 10°, 20° and zenith, and the relative solar azimuth angle (i.e., the horizontal projection of the angle between sun and the measurement viewing direction, RSAA) is always 90°. The asymmetry parameter (g) of the aerosol layer in the PBL has been chosen to be 0.68, which is a typical value for urban aerosols. The single-scattering albedo (SSA) was set to 0.95 and the surface albedo to 0.13. Figure 3 shows that with low AOD (pristine conditions) all elevation angles have different values, and beginning with a certain AOD, aerosol forces the convergence, starting with the lowest elevation angles (considering a typical DOAS error for the dSCD of 10 %). This means that the collapsing of the dSCDs of the lowest elevation angles can be seen in the correction factors when the AOD reaches a certain value, and the collapsing with even higher elevation
angles investigated in this paper, as well as in other studies (Volkamer et al., 2009; Sinreich et al., 2010).

For the VMR retrieval, the plateau of the correction factors of a (low) elevation angle must be identified. The mean value of a plateau of a certain elevation angle (and not the single correction factor value).

This general behavior of the correction factors can be seen in all wavelengths, layer heights and different solar zenith angles investigated in this paper. It is also observable that in the range of collapsing, the actual correction factor does not change much in value and shows a kind of plateau. This means that once convergence is observed, a further increase in aerosols has limited effect and the effective path length scales linearly with the observed O_AOD. Additionally, in some cases a small slope even in the plateau range could be observed, which could be due to multiple scattering in the lowest layer. Thus, unrealistically high AOD values should not be considered in this method; however, if the upper limit is chosen too low, it only has a small effect on the value of the correction factor.

The correction factors in Fig. 4 are plotted versus SZA and are derived from 3° elevation angle data for the layer heights of 0.5, 1 and 2 km – i.e., constant trace gas mixing ratios up to the corresponding height (box profile). In order to create a diurnal plot, the morning values of the solar zenith angle are negative. Yet the values are symmetric towards 0° SZA, showing “tooth shapes” (caused by the pronounced forward scattering on aerosols in the zenith reference). This symmetry is owing to the constant azimuth angle, and as shown in Sect. 3.1, the plot can become significantly asymmetric with changing azimuth angle (or changing layer height, or both). The errors represent the statistical error, i.e., the standard deviation within the plateaus. It can be seen that, for most SZA, the correction factors vary within ±20% in the worst case (500 m and 360 nm). For a 2 km layer at 630 nm the variation is very small (±5%). Also, the higher the layer and the larger the wavelength, the less sensitive the correction factors become towards the actual layer height. The relative difference of the correction factor between different layer heights is largest for the shortest wavelength at 360 nm. A doubling from 0.5 km to 1 km leads to an increase by 1.5 and from 1 km to 2 km by a factor of 1.2 to 1.3 during the day (SZA ≤ 70°). For 630 nm, the corresponding factors are 1.0 to 1.2 and 1.0 to 1.1, which are much lower.

These correction factors are calculated for clear-sky conditions. In the case of clouds directly above the PBL, the correction factors tend towards unity (independently of the layer height).

Also, it can occur that the aerosol layer and the trace gas layer are decoupled in the way that the aerosol layer extends to higher altitudes than the trace gas layer (e.g., in the case of a residual layer from the previous day(s) that is depleted in emission-related reactive gases such as NOx). Figure 5 shows correction factors of such a scenario (which are retrieved the same way as before): while the trace gas profile layer height (NOx) is always fixed to 500 m, the box profile aerosol layers are assumed for different heights of 500 m, 1000 m, 2000 m and 3000 m (thick lines) for three different SZA (20°, 50° and 80°). For comparison, the dotted lines represent the scenario that the NOx layer extends to the same height as the aerosol layer; this means that both layer heights are 500 m, 1000 m, 2000 m or 3000 m. These calculations were made for the MCMA-2006 case study (assuming an RSAA of 90°), which is described in the next chapter.
Fig. 4. Correction factor mean values for different PBL heights (0.5 km, 1 km and 2 km) and for the wavelengths (a) 360 nm, (b) 477 nm, (c) 577 nm and (d) 630 nm versus solar zenith angle. An AOD range between 0.3 and 0.6 (3° elevation angle) was used to derive the mean values. For further discussion see text.

Comparing the thick lines with the dotted ones, it is obvious that the correction factors of a fixed trace gas layer do not follow the increase of the correction factors of expanding collocated layers to the same extent. The increase is much more moderate (< 30%) when the trace gas layer is fixed to 500 m and only the aerosol layer expands. In the case of 50° SZA, this increase is even smaller than 15%. In contrast, the increase of the correction factors of collocated layers is smaller than 65% for SZA = 50° and smaller than 170% for SZA = 80°. For 20° SZA the correction factor doubles with a (trace gas and aerosol) layer increase from 500 m to 3000 m. This shows that the main determinant is the trace gas layer, and that the actual height of a larger aerosol layer plays a secondary role.

While this method largely eliminates the sensitivity to the AOD, the sensitivity towards other parameters of the atmospheric state and measurement geometry still applies. The variability of the correction factor is investigated in more detail in the next chapter with the MCMA-2006 MAX-DOAS measurements as example.

3 MCMA-2006 case study

3.1 Correction factors for the MCMA-2006 MAX-DOAS setup

The correction factors in this section are calculated for the example of Mexico City, which is located at about 2200 m above sea level. In 2006, during the MCMA-2006
measurement campaign, MAX-DOAS measurements were performed at the “T0 site” at about 16 m height on the roof top of the Instituto Mexicano del Petroleo (IMP, a four-level building), which is located at the north edge of downtown Mexico City. The retrieved dSCDs of NO₂ and O₃ of 1° and 3° elevation angle are applied to the parameterization method after they were filtered with regard to overlapping. For both species, an uncertainty in the dSCDs of 10% is tolerated. For the calculation of the correction factors the radiative transfer model McArtim is initiated using values for surface albedo (0.09), single-scattering albedo (0.78) and asymmetry parameter (0.68) as measured for urban pollution in Mexico City (Barnard et al., 2008). The O₃ dSCD is retrieved from the 360 nm absorption band and the NO₂ dSCD from a DOAS fitting in wavelength range between 368 nm and 390 nm.

For the example of the MCMA-2006 measurements, an AOD between 0.3 and 0.6 is a good range for layer heights from 500 m to 3000 m to reflect the overlapping of the observed 1° and 3° elevation angles. Also, at times, overlapping of higher elevation angles could be observed for both O₃ and NO₂, indicating a higher AOD. However, due to the plateau formation, a higher AOD typically has only a small effect on the correction factor. Therefore, mean values over the mentioned AOD range were used as correction factors, which are applied to the MAX-DOAS dSCDs in Sect. 3.2.

For this method, it is necessary to know or at least estimate the PBL height. Mexico City is known for its dynamic PBL, and in extreme cases of PBL variability, the correction factor can vary by a factor of 3 over the course of a day. As shown in the last section, accurate knowledge of PBL height is more crucial in the morning when the PBL height is lower. Here, a typical diurnal PBL height cycle was estimated to be about 500 m until 09:00 (local time), then to rise up constantly until 2500 m at 15:00, and stay at this height until the end of the day (see inset of Fig. 6). This is compatible with measurements of the PBL made by de Foy et al. (2005) in MCMA-2003 and by K. Knupp and D. Phillips from The National Space Science & Technology Center of the University of Alabama at Huntsville in MCMA-2006. The measurement method of K. Knupp and D. Phillips is based on a ground-based RADAR profiler, and is described in Knupp et al. (2006).

For the MCMA-2006 case study, the variability of the correction factor is investigated in some more detail. While this method largely eliminates the sensitivity to the AOD the sensitivity towards other parameters of the state of the atmosphere and measurement geometry still applies, as seen above for the case of the PBL height. Most important parameters are here RSAA, surface albedo (SA), g and SSA. Table 1 lists the relative change of the correction factor of the three latter parameters for different PBL heights (PBLh) and SZA when applying the corresponding parameter and leave the others at standard values (SA=0.09; g = 0.68; SSA = 0.78). The error is a statistical error resulting from the standard deviations when retrieving the plateau values. The RSAA, which is important since aerosols scatter light preferably in forward direction, is investigated separately further below.

As can be seen, all virtual changes are below 10%, and thus only play a minor role for the derivation of the mixing ratios. An exception is the asymmetry parameter for low layer heights for which changes are smaller than 15%.

The dependence of the correction factor on the RSAA was considered for the MCMA-2006 MAX-DOAS setup specifically. The MAX-DOAS measurements collected light simultaneously from the north, west and south (about 7° rotated clockwise to the exact geographical directions). The radiative transfer calculations were made with the corresponding RSAA depending on the time of the day. The correction factors considering azimuth effect and diurnal PBL dynamics are plotted in Fig. 6 (upper panel) versus the SZA (morning values are minus). No measurements were performed in east direction, but calculations in east direction are added here to demonstrate the azimuth effect. While in the afternoon the correction factors of all 4 directions in Fig. 6 are very similar, they show significant differences when PBL and RSAA are low (east and south in the morning). The north and west direction values show a morning increase (also due to the expansion of the PBL) that is hardly affected by an azimuth effect. The lower panel of Fig. 6 illustrates the RSAA for the four directions. Since the lowest SZA during
the measurement campaign was around 15°, no values for the RSAA at −10° and +10° are available. Thus, for the calculation of the ±10° SZA correction factors, the RSAA mean values of −20° and +20° were taken.

Figure 6 shows that measuring towards the sun has a larger effect on the correction factors the lower the PBL is. This is qualitatively consistent with the $g$ dependence on the PBL height shown in Table 1.

### 3.2 Determination of MAX-DOAS VMRs and comparison with LP-DOAS during MCMA-2006

The correction factors from Fig. 6 were used to convert the NO$_2$ dSCDs into NO$_2$ VMRs by means of corresponding O$_4$ dSCDs using 1° and 3° elevation angle and applying Eq. (5). The dSCDs were retrieved by analyzing the spectra relative to the closest zenith reference measured prior to the acquisition of the measurement spectrum. Also, the corresponding ring spectrum was used so that reference and ring spectrum were continuously updated. For 3 arbitrary days (23–25 March 2006), the dSCDs in south direction are plotted in Fig. 7 for (b) NO$_2$ and (c) O$_4$. The overlapping of the lowest elevation angles can be seen clearly. Figure 7a shows the corresponding mixing ratio time series of MAX-DOAS in south direction for the same days. Thereby only dSCDs were used that fulfill the detection limit. It was set to 2 times the root mean square of the fit residual divided by the strongest convolved (differential) cross-section peak in the respective analysis wavelength window. Additionally, only dSCDs were considered whose spectra were acquired at SZA not larger than 80°. Also, VMR values of two LP-DOAS measurements from the same site pointing to the south and to the northwest with retro-reflectors at about 2.6 km and 1 km distance, respectively, are shown in Fig. 7a (Merten, 2008). During daylight (SZA < 90°, light-yellow background in Fig. 7a), a general agreement in the

![Fig. 7](https://example.com/figure7.png)

**Fig. 7.** (a) Comparison of MAX-DOAS pointing south and LP-DOAS pointing south and northwest for 3 arbitrary days. The light-yellow background indicates daylight (SZA < 90°). The corresponding dSCD for (b) NO$_2$ and (c) O$_4$ are shown in the panels below.
shape can be seen. However, for MAX-DOAS the peak on 23 March is not as high as for LP-DOAS. LP-DOAS shows in average about 1.7 times more NO$_2$ than MAX-DOAS. At the time of the peak (09:35), the PBL was assumed to be about 700 m. The layer height in this approach would have needed to be around 300 m in order to match the NO$_2$ VMR of LP-DOAS. Assumably, this difference is mostly a vertical inhomogeneity. On 24 March some scatter can be seen for both MAX-DOAS and the two LP-DOAS. Also, differences between the two LP-DOAS are observable several times, indicating horizontal inhomogeneities.

In order to assess the diurnal behavior for the overall time series, in the following, half-hourly medians are taken for the time when all three instruments conducted measurements (10 March–1 April 2006). Figure 8 compares the mixing ratios of MAX-DOAS of all directions and of LP-DOAS of both directions each for 1° (upper panel) and 3° (lower panel). The values are plotted as whiskers with crosses indicating medians, and vertical extensions the 25 and 75 percentiles of the values. The MAX-DOAS whiskers represent the statistics from all three viewing directions. Additionally, the values of the individual MAX-DOAS directions are plotted as lines, which show a small horizontal variability only between 10:30 and 12:30 in both 1° and 3°. For the rest of the median diurnal profile, the values of the 3 directions lie mainly on top of each other, which is a confirmation of the calculated azimuth effect shown in Fig. 6. In general, the MAX-DOAS and LP-DOAS values show good agreement. However, the LP-DOAS has significantly higher values than MAX-DOAS in the afternoon, when the mixing in the PBL is less active and O$_3$ concentrations are typically high (Volkmann et al., 2010). This is slightly more pronounced in the case of 3° elevation angle than in 1° elevation angle, which indicates a vertical gradient. Also, the values of the two LP-DOAS directions temporarily differ by a factor of 2 although the MAX-DOAS values of the three directions mostly agree with each other. Despite the relatively strong scatter in the LP-DOAS values, it indicates that there are horizontal gradients which are not detected by MAX-DOAS. Hence, it must only happen below the MAX-DOAS line of sight of 1° elevation angle, thus in the lowest couple of 10 m (see Fig. 10).

In Fig. 9 the horizontal (left panel) and vertical (right panel) extent of the air masses probed by the MAX-DOAS measurements for 1° (upper panel) and 3° (lower panel) elevation angle is plotted. This is the differential effective path length and its vertical projection (see Eq. 3), which represents the spatial fetch of the MAX-DOAS measurements. The horizontal lines indicate the distances from the light source to the respective retro-reflectors for the LP-DOAS measurements. It can be seen in Fig. 9 that until 11:00 the MAX-DOAS at the measured wavelength and the longer LP-DOAS light path have about the same horizontal expansion. Due to the rising of the PBL and the involved dilution of aerosols, the differential effective path length increases continuously over the course of the day and reaches about 2–3 times the horizontal path during afternoons. As expected from the approach description in chapter 2, the horizontal path length is comparable for 1° and 3° elevation angle.

The same general picture can be observed with the median top height of the differential effective path, $h_{\text{eff}}$, which represents the vertical extent over which the box-averaged VMR is measured. The median day starts with values for $h_{\text{eff}}$ around 40 m (1°) and 130 m (3°) vertical dimension increasing during the day to about a factor of 3 to reach about 100 m (1°) and 300 m (3°) in the afternoon. The measurements were performed on roof-top level so that these heights start at a measurement altitude of about 16 m above ground.

By combining Fig. 8 with Fig. 9, Fig. 10 is drawn showing median NO$_2$ VMRs for MAX-DOAS 1° and 3° elevation angle as well as LP-DOAS. This is done for the south direction at a time period from 08:30–09:00 (red), 12–12:30 (green), and 15:30 to 16:00 (blue). The LP-DOAS NO$_2$ VMRs (squares) are plotted at roof-top level of 16 m height. The 1° elevation angle MAX-DOAS VMR values (circles) are at half altitude of the effective scattering height. The highest points (triangles) are retrieved from 3° elevation angle.
Fig. 9. Horizontal (a and c) and vertical (b and d) expansion of the MAX-DOAS measurements for 1° (a and b) and 3° (c and d) elevation angle.

angle MAX-DOAS data minus the 1° elevation angle data weighted by the respective effective scattering heights as follows:

\[
\text{VMR}^* = \frac{\text{VMR}(3°) \cdot h_{\text{eff}}(3°) - \text{VMR}(1°) \cdot h_{\text{eff}}(1°)}{h^*},
\]

with \( h^* \) being the height of the triangular points and the value at half height of the difference in 3° elevation angle and 1° elevation angle \( h_{\text{eff}} \) above the 1° elevation angle layer, which is \( h_{\text{eff}}(1°) + \frac{h_{\text{eff}}(3°) - h_{\text{eff}}(1°)}{2} \). This ensures that the values in Fig. 10 represent non-overlapping layers and that only the mixing ratio retrieved in the respective layer is shown.

In the morning, a slight vertical increase between LP-DOAS and MAX-DOAS can be seen that becomes a slight decrease at midday. However, the values are mostly within the error tolerance. In the afternoon, a significant vertical gradient can be observed, which halves the VMR from 16 m to about 240 m altitude, which is more pronounced closer to the ground. A similar vertical gradient was observed for toluene and C\(_2\)-alkylbenzene during MCMA-2003 in Mexico City by Jobson et al. (2010) by a factor of 2 in 21 m difference from the ground. This might indicate that the gradient shown here also continues down to the ground.

4 Conclusions

A parameterization method to convert MAX-DOAS dSCDs into near-surface box-averaged VMRs is described in detail. Differential effective light paths were calculated, and correction factors are derived from radiative transfer modeling to retrieve near-surface trace gas mixing ratios. For applying this method, the aerosol load must be high enough (typically an AOD of 0.3 or higher), as indicated by the “collapsing” of O\(_4\) dSCD values in the lowest elevation angles (i.e., they have about the same value). Such conditions are often found in the marine boundary layer, or in urban polluted atmospheres. Then the method is rather insensitive to the assumptions about the state of the atmosphere (aerosol extinction, phase function, surface albedo, etc.). However, especially the actual trace gas layer height and relative solar azimuth angle (RSAA) have a strong impact in cases when both RSAA and planetary boundary layer (PBL) are low. The VMRs retrieved by this method become more variable with decreasing PBL, and therefore the application of this method is not recommended for low PBL layer heights (e.g., below 500 m) without knowing the actual height.
The presented approach has in particular several advantages:

1. The approach is straightforward (a one-step conversion) and significantly reduces computational effort. It retrieves ~1 degree of freedom (near-surface volume mixing ratio), which is about half of the typical information content (between 1.8 to 2.1 degrees of freedom) that can be derived from a full inversion; see Clemer et al. (2010).

2. The approach focuses on those altitudes where MAX-DOAS is maximally sensitive and least limited in information content, which is close to instrument altitude. This near-surface concentration can serve as an anchor for the a priori estimate in the lowest layer, although it does not provide independent information in the optimal estimation retrieval.

3. It only depends weakly on the aerosol layer height and not on the actual aerosol load (as long as the O$_4$ dSCD values of the lowest elevation angles “collapse”), which is typically necessary for MAX-DOAS concentration retrievals.

4. To apply this method, the trace gas layer height is ideally known, or otherwise has to be estimated. The near-surface VMR becomes rather insensitive of trace gas layer height if this height is 1 km or higher. Then, if the layer height was twice as high as assumed (e.g., 2 km), the error in the VMR estimate is 30% or less. The method is most insensitive to layer height in high PBLs.

5. If the trace gas dSCDs of the lowest elevation angles “collapse” within DOAS error, the trace gas profile can be approximated reasonably as a box profile.

During the MCMA-2006 measurement campaign, two LP-DOAS facing in near-opposite directions and a MAX-DOAS pointing in three directions perpendicular to each other were deployed in a systematic effort to access inhomogeneities of the Mexico City air mass. While LP-DOAS averages the trace gas concentration close to the roof top (a few meters above street canyons) with a horizontal expansion of 1 and 2.6 km, MAX-DOAS covers a minimum spatial fetch of 40 m height and 2.5 km horizontal length in the morning (1° elevation angle) up to a maximum of about 350 m height and 5 km length in the evening (3°). For the 3° elevation angle data, as expected the vertical extension is about 3 times higher than that of the 1° elevation angle data. The comparison of the LP-DOAS and MAX-DOAS values gives indication of horizontal and vertical inhomogeneities. In particular, a vertical gradient of NO$_2$ close to the ground can be concluded in the afternoon. The comparison shows the unique potential and importance of MAX-DOAS measurements in dynamic polluted environments like megacities.

Supplementary material related to this article is available online at: http://www.atmos-meas-tech.net/6/1521/2013/amt-6-1521-2013-supplement.pdf.

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