Title
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Permalink
https://escholarship.org/uc/item/2qc3q753

Journal
Monthly Notices of the Royal Astronomical Society, 454(2)

ISSN
0035-8711

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Publication Date
2015-12-01

DOI
10.1093/mnras/stv2072

Peer reviewed
Forged in FIRE: cusps, cores, and baryons in low-mass dwarf galaxies

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20 October 2015

ABSTRACT

We present multiple ultra-high resolution cosmological hydrodynamic simulations of \(M_* \sim 10^{1-6.3} M_\odot\) dwarf galaxies that form within two \(M_{\text{vir}} = 10^{9.5-10} M_\odot\) dark matter halo initial conditions. Our simulations rely on the FIRE implementation of star formation feedback and were run with high enough force and mass resolution to directly resolve structure on the \(\sim 200\) pc scales. The resultant galaxies sit on the \(M_*\) vs. \(M_{\text{vir}}\) relation required to match the Local Group stellar mass function via abundance matching. They have bursty star formation histories and also form with half-light radii and metallicities that broadly match those observed for local dwarfs at the same stellar mass. We demonstrate that it is possible to create a large (\(\sim 1\) kpc) constant-density dark matter core in a cosmological simulation of an \(M_* \sim 10^{4} M_\odot\) dwarf galaxy within a typical \(M_{\text{vir}} \sim 10^{10} M_\odot\) halo – precisely the scale of interest for resolving the Too Big to Fail problem. However, these large cores are not ubiquitous and appear to correlate closely with the star formation histories of the dwarfs: dark matter cores are largest in systems that form their stars late (\(z \lesssim 2\)), after the early epoch of cusp building mergers has ended. Our \(M_* \sim 10^{4} M_\odot\) dwarf retains a cuspy dark matter halo density profile that matches that of a dark-matter only run of the same system. Though ancient, most of the stars in our ultra-faint form after reionization; the UV field acts mainly to suppress fresh gas accretion, not to boil away gas that is already present in the proto-dwarf.

Key words: galaxies: formation — galaxies: evolution — galaxies: dwarf — cosmology: theory — methods: numerical

1 INTRODUCTION

Many of the most pressing problems associated with the standard LCDM paradigm concern the faintest \(M_* \sim 10^9 M_\odot\) dwarf galaxies and the dark matter halos that have the right abundance to host them: \(M_{\text{vir}} \sim 10^{10} M_\odot\) (Garrison-Kimmel et al. 2014; Brook et al. 2014). If LCDM is correct, then the dark matter halos hosting these dwarfs must be extremely inefficient at converting baryons into stars (Klypin et al. 1999) and they also must be significantly less dense in their centers than predicted in dissipationless LCDM simulations (Boylan-Kolchin et al. 2011, 2012; Ferrero et al. 2012; Garrison-Kimmel et al. 2014; Tollerud et al. 2014; Klypin et al. 2014; Papastergis et al. 2015). This latter issue (known as the Too Big to Fail problem) may be related to indications that dwarf galaxies reside within dark matter halos that have cored density profiles rather than the cuspy NFW-like profiles predicted in CDM simulations (Flores & Primack 1994; Kuzio de Naray et al. 2008; de Blok et al. 2008; Oh et al. 2008; Walker & Peñarrubia 2011; Salucci et al. 2012; Amorisco et al. 2014; Ogiya & Burkert 2015 but see Strigari et al. 2014).

While some authors have taken these discrepancies as motivation to explore non-standard dark matter models (Macciò & Fontanot 2010; Vogelsberger et al. 2012; Rocha et al. 2013; Horiuchi et al. 2014; Governato et al. 2015), others have argued that that it may be possible to naturally resolve them through a better understanding of star formation and feedback in low-mass galaxies. Specifically, the inefficiency of dwarf galaxy formation is believed to be driven by supernovae feedback and the effects of an ioniz-
Reproducing even the broad-brush properties of dwarfs in a cosmological framework, regardless of their internal structure, has been historically challenging. At these scales, the relationship between stellar mass and halo mass derived from local galaxy counts (Garrison-Kimmel et al. 2014; Brook et al. 2014) implies a suppression of galaxy formation by a factor of about 1000. While it is generally believed that stellar feedback is the main agent responsible for this suppression, actually getting a physically realistic model of the relevant processes to manifest these expectations has proven difficult.

The past several years have proven fruitful in this regard, with many published studies achieving substantial suppression in the conversion of baryons to stars on the scale of dwarf galaxy halos (Governato et al. 2010; Sawala et al. 2011; Simpson et al. 2013; Munshi et al. 2013; Governato et al. 2015; Trujillo-Gomez et al. 2015). As we show below, however, many of these studies have not quite reached the level of suppression that seems to be required by local galaxy counts. Moreover, whether or not these feedback models also match the different observed scaling relations for these systems (Wolf et al. 2010; Kirby et al. 2013; Collins et al. 2014) is still not clear. Reproducing both the correct stellar mass and structural properties has proven to be an even more difficult challenge (Sales et al. 2010). The observed stellar metallicity - stellar mass tight correlation (Gallazzi et al. 2005; Kirby et al. 2013) can also put very important constraints on the feedback models and how these are implemented.

As for the question of feedback-driven core formation, much remains debated. Some of the most successful simulations at producing cores in dwarf galaxies have suggested a transition mass below $M_* \sim 10^7 M_\odot$ where core formation becomes difficult (Governato et al. 2012). Using a slightly different set of simulations, Di Cintio et al. (2014) find similar results, and suggest that the cusp-core transition should be most effective when the ratio of stellar mass to dark matter halo mass relatively high, in massive dwarfs with $M_* \sim 10^8 M_\odot$ and $M_{\text{vir}} \sim 3 \times 10^{10.5} M_\odot$. Importantly, they also find that cuspy profiles are retained for the $M_* \sim 10^6 M_\odot$ dwarfs of concern (residing in $M_{\text{vir}} = 10^{10.5} M_\odot$) although resolution may have been an issue in these cases. At some mass scale, galaxy formation may become effectively stochastic (e.g., Boylan-Kolchin et al. 2011). Recent work by Sawala et al. (2015, 2014), however, suggests that the scale at which stochasticity becomes important is somewhat lower ($M_{\text{vir}} \sim 10^9 - 10^{10} M_\odot$).

Though the results of Di Cintio et al. (2014) and Governato et al. (2012) agree reasonably well, a different set of high resolution simulations with a simpler implementation of stellar feedback have not produced cores in dwarf galaxy halos at any mass (Vogelsberger et al. 2014), even though a number of other observables are well matched. The absence of cores produced by stellar feedback in these simulations could be due to the fact that their sub-grid ISM and star formation model leads to star formation histories that are (likely) artificially smoothed in time, compared to the bursty star formation histories found in more explicit models (Hopkins et al. 2014; Muratov et al. 2015). Conversely, Trujillo-Gomez et al. (2015) found that radiation pressure from massive stars was the most important source of core formation in their simulations, not thermal feedback from supernova, which has been the primary mode used by other groups that have produced cores. More generally, models for feedback that have been used up until now have been sub-grid and necessitated ad-hoc approximations, such as turning off cooling for material heated by SNe. As such it is not clear whether the feedback we actually expect from stellar evolution models is capable of producing large cores, or whether the mass-limit for core formation is robust.

In this paper, we attempt to minimize the freedom of sub-grid galaxy formation models and to incorporate as many important physical processes in a manner that is as realistic as possible present in order to understand if and how star formation affects the gravitational potential wells of dwarf dark matter halos. To these ends, we have conducted a series of high resolution cosmological hydrodynamical simulations of two dwarf halos using the code presented in Hopkins et al. (2014). In this work, we showed that this implementation of stellar feedback successfully reproduces the observationally-inferred relationship between the stellar mass-dark matter halo mass ($M_* - M_{\text{halo}}$) and star formation histories of galaxies at all redshifts where observational constraints are currently available. Faucher-Giguere et al. (2015) recently showed that it also replicates the neutral hydrogen content of high-redshift halos.

To our knowledge, the set of simulation presented here include the current highest resolution simulation of this type with an explicit implementation of feedback yet achieved. This not only facilitates a more accurate treatment of astrophysical processes but is also crucial in the context of dwarfs as dark matter probes. The dwarfs of concern have half-light radii of $\sim 500$ pc, and thus any dark matter core of relevance needs to be dynamically resolved at this scale. According to well-documented convergence test studies (Power et al. 2003), many previous simulations that have reported core formation on this scale were quite poorly resolved, some at only $\sim 2 - 3$ softening lengths. In what follows we make every effort to clarify our resolution limitations.

The paper is organized as follows. In Section 2 we describe the computational methods which we have used and our choice of initial conditions. We present the results of our simulations in Section 3. We pay closer attention to the matter content of our simulated dwarfs, and the possible formation of cores, in Section 4. We conclude with a summary where we discuss the achievements and shortcomings of the simulations in Section 5.

2 SIMULATIONS

We have run a series of multimass cosmological hydrodynamical simulations (Porter 1985, Katz & White 1993) following the formation and evolution of structure in the $\Lambda$CDM model of two dwarf galaxy halos. Each simulation is a cosmological zoom-in that includes high-resolution gas and dark matter for the flow converging region that generates the main object. The rest of the simulation box is sampled by low-resolution dark matter particles that account for tidal forces. The cosmological model adopted throughout this paper is based on cosmic microwave background results (Komatsu et al. 2011): $\sigma_8 = 0.801$, $\Omega_m = 0.734$, $\Omega_b = 0.266$, $\Omega_{\Lambda} = 0.0449$, $\alpha_b = 0.963$ and $h = 0.71$.

To generate the cosmological initial conditions we made use of MUSIC, an OPENMP parallel algorithm to generate multi-scale
initial conditions with multiple levels of refinements for cosmological “zoom” simulations (MUSIC [Hahn & Abel 2011]) and we followed the method outlined in Oñorbe et al. (2014). To select our dwarf candidates we first run a medium-resolution dark-matter only cosmological simulation using GADGET-2 [Springel 2005] with a cubic volume of 7 Mpc on a side with particle mass \( m_p = 9.7 \times 10^6 M_\odot \) and Plummer equivalent force softening length of 176 pc. To be able to study the main statistical properties of dwarf galaxy halos we also run a bigger dark-matter only simulation of 35 Mpc on a side with particle mass \( m_p = 1.2 \times 10^7 M_\odot \) and Plummer equivalent force softening length of 563 pc. In this work we present simulations of two dwarf galaxy halos, one with a virial mass of \( M_{\mathrm{vir}} = 3.2 \times 10^9 M_\odot \) and the other with \( M_{\mathrm{vir}} = 9.2 \times 10^9 M_\odot \).

Based on our analysis of the 35 Mpc simulation, we have chosen our dwarf candidates to lie as close as possible to the mean values of spin, concentration and halo formation time for its mass while still having a small Lagrangian volume (see Oñorbe et al. 2014). The specific values of these parameters for our two halos can be found in Table 1. We point to Appendix A for a more detailed description of these parameters and how they compare with a sample of halos in the same mass bin.

To check the convergence of our results we have run two resolution levels for our simulations: in our low-resolution hydrodynamical testing runs we use a dark matter particle mass of \( 1.01 \times 10^4 M_\odot \) and a particle gas mass of \( 2.04 \times 10^3 M_\odot \) (the mass resolution for the collisionless run is therefore \( 1.22 \times 10^4 M_\odot \)). The high resolution runs used a dark matter particle mass of \( 1.26 \times 10^4 M_\odot \) and a gas particle mass of \( 254 M_\odot \) (the particle resolution for the collisionless run is therefore \( 1.5 \times 10^3 M_\odot \)). None of the high resolution regions of the simulations presented in this work are contaminated by low resolution particles at any redshift within 1.6 virial radii.

The simulations presented in this paper use GIZMO [Hopkins et al. 2012, 2013, 2014] run in P-SPH mode which include physical models for star formation and stellar feedback presented in Hopkins et al. (2014). Two of the runs presented here Ultrafaint and Dwarf_early were also presented in Hopkins et al. (2014) (m09 and m10 respectively). We summarize their properties below, but readers interested in further details (including resolution studies and a range of tests of the specific numerical methodology) should see Hopkins et al. (2012, 2013, 2014).

For the halo identification in the simulation we have used the public code Amiga Halo Finder (AHF [Knollmann & Knebe 2009]), an MPI parallel code for finding gravitationally bound structures in simulations of cosmic structure. Results presented in this work use a highest density peak+sigma-clipping method to find the center. We have also tested different centering algorithms to confirm that our results do not depend on which method was used.

### 2.1 Numerical Methods

The P-SPH method adopts the Lagrangian “pressure-entropy” formulation of the SPH equations developed in Hopkins (2013); this eliminates the major differences between SPH, moving mesh, and grid (adaptive mesh) codes, and resolves the well-known issues with fluid mixing instabilities in previously-used forms of SPH (e.g. Agertz et al. 2007; Sijacki et al. 2012). P-SPH also manifestly conserves momentum, energy, angular momentum, and entropy. The gravity solver is a heavily modified version of the GADGET-3 [Springel 2005] hybrid tree-particle mesh (Tree-PM) method; but GIZMO also includes substantial improvements in the artificial viscosity, entropy diffusion, adaptive timestepping, smoothing kernel, and gravitational softening algorithm, as compared to the “previous generation” of SPH codes. These are all described in detail in Hopkins (2013); Hopkins et al. (2014). In particular, in “traditional” GADGET, softenings are not adaptive, and pairwise interactions are simply smoothed by the larger of the two particle softenings. We have also modified the softening kernel as described therein to represent the exact solution for the potential of the SPH smoothing kernel. Therefore our “standard” simulations use adaptive gravitational softening lengths for gas which minimum is a factor \( \sim 10 \) smaller than the fixed dark matter gravitational softening lengths.

In order to test this approach we have also run the same initial conditions using identical softenings for both the baryonic and dark matter particles (close to the higher dark matter default value). We labeled these runs according to the late star formation history of the high resolution runs (see Table 1 and the discussion below for more details).

In our simulations, gas follows an ionized+atomic+molecular

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1. Unless otherwise stated, in this paper we define the virial overdensity using the spherical top hat collapse approximation by Bryan & Norman (1998).
2. [http://www.tapir.caltech.edu/~phopkins/Site/GIZMO]
cooling curve from $10 - 10^{10}$ K, including metallicity-dependent fine-structure and molecular cooling at low temperatures, and high-temperature ($\gtrsim 10^4$ K) metal-line cooling followed species-by-species for 11 separately tracked species. At all times, the appropriate ionization states and cooling rates are tabulated from a compilation of CLOUDY runs, including the effect of a uniform but redshift-dependent photo-ionizing background computed in Faucher-Giguère et al. [2009] together with local sources of photo-ionizing and photo-electric heating. Self-shielding is accounted for with a local Sobolev/Jeans-length approximation (integrating the local density at a given particle out to a Jeans length to determine a surface density $\Sigma$, then attenuating the background seen at that point by $\exp(\kappa_n \Sigma)$).

Star formation is allowed only in dense, molecular, self-gravitating regions above $n > n_{\text{crit}}$ ($n_{\text{crit}} = 100 \text{ cm}^{-3}$) for our high-resolution simulations. This threshold is much higher than that adopted in most “zoom-in” simulations of galaxy formation (the high value allows us to capture highly clustered star formation). We follow Krumholz & Gnedin [2011] to calculate the molecular fraction $f_{\text{H}_2}$ in dense gas as a function of local column density and metallicity, and allow SF only from molecular gas. We also follow Hopkins et al. [2013] and restrict star formation to gas which is locally self-gravitating, i.e. has $\alpha = \delta t^2 \delta r / G M_{\text{gas}} (< \delta r) < 1$ on the smallest available scale ($\delta r$ being our force softening or smoothing length). This forms stars at a rate $\rho_s = \rho_{\text{normal}} / \tau_{\text{ff}}$ (i.e. 100% efficiency for free-fall time); so that the galaxy and even kpc-scale star formation efficiency is not set by hand, but regulated by feedback (typically at much lower values).

Feedback from stellar evolution is modeled by including energy, momentum, mass, and metal return from radiation, supernovae, stellar winds, and photoionization. Every star particle is treated as a single stellar population, with a known age, metallicity, and mass. Then all feedback quantities (the stellar luminosity, spectral shape, SN rates, stellar wind mechanical luminosities, metal yields, etc.) are tabulated as a function of time directly from STARBURST99 stellar population synthesis model [Leitherer et al. 1999], assuming a Kroupa [2002] IMF. Details on the implementation of each of these physical processes in our simulations can be found in Hopkins et al. [2014]. No black hole physics has been considered in these simulations.

Despite taking all our inputs directly from stellar population models, there are some ambiguities in how we implement them. For example, when we deposit mass, momentum, and energy to particles within the SPH kernel, we can do so according to a mass-weighting or volume-weighting scheme. We have experimented with both, and we refer to these options as Feed-M and Feed-V, respectively.

We stress that the systematic differences due to these (and other similar) purely numerical choices (see Appendix A of Hopkins et al. [2014]) are relatively small for integrated quantities like the stellar mass. However, since the dynamics of galaxies and star formation are chaotic, a small perturbation can make a non-negligible difference to the shape of the star formation history. These essentially stochastic variations will provide a useful means for us to examine the role of different star formation histories in shaping cores.

We have found that the main global parameters describing the dwarf galaxies are quite robust regardless of resolution, softening and other minor changes in the code. See Appendix B for a full discussion on the convergence of our results.

### 2.2 Sample Summary

A summary of all the relevant parameters used in the ultra high resolution runs presented in this work is shown in Table 1 along with the naming conventions we have adopted. In this work we present a total of six high resolution simulations of two dwarf galaxy halos, one with a virial mass of $M_{\text{vir}} = 3.2 \times 10^9 M_{\odot}$ and the other with $M_{\text{vir}} = 9.21 \times 10^9 M_{\odot}$ (as measured in the high-resolution collisionless simulations). For the more massive halo we present here four runs, a high resolution collisionless run (Dwarf_dm) and a total of three different hydrodynamical runs which include two feedback implementation tests and the softening test mentioned above.

We have named the three hydrodynamical Dwarf simulations based on their star formation histories (see section 3.2 below). The run we call “Dwarf_early” shows most of its star formation at early times and corresponds with the feedback method Feed-V. The run we call “Dwarf_late” uses feedback method Feed-M and shows a more significant star formation rate at low redshifts. The “Dwarf_middle” run is the softening test which uses feedback method “Feed-M” and its star formation rate history stands just between the two. Simulations of the same dwarf using the “Meshless Finite Mass” method implemented in GIZMO [Hopkins 2014] and the feedback Feed-V method produce results very similar to the “Dwarf_early” run presented here (Fitts et al., in preparation).

For the smaller halo we have run the same number of simulations as we have for the larger one, but their results were so similar that we present only one hydrodynamic run (Ultrafaint, which uses Feed-V) and one collisionless run (Ultrafaint_dm). The hydrodynamical runs Dwarf_early and Ultrafaint were already presented in the first FIRE paper (Hopkins et al. 2014).

As pointed out above, we have also checked the convergence of these results with resolution by running all these setups also at a lower resolution level. We discuss these runs in detail in Appendix B. We have also run many more ($\sim 50$) simulations at this lower resolution level of these halos to test other purely numerical issues and the effects of adding/removing each feedback mechanism in turn. Some of these are summarized in Hopkins et al. [2014]. We will not discuss them further in this paper because they are either not instructive for the study of this work because the included physics is not complete or because there is no change in the results. Even given excellent force and mass resolution, the timestep criterion used in simulations is always a concern if many, many orbits of N-body particles must be followed (as in the halo centers of the systems studied here). These can artificially deteriorate a central cusp, if an insufficiently stringent timestep criterion and/or error tolerance for the long-range force computations is used. We have therefore re-run a subset of our low-resolution runs, making the timestep criterion a factor of $\sim 30$, and force error tolerance a factor of $\sim 100$ times more strict than our default choices. This amounts to taking $< 100$ year timesteps, with a tree force accuracy a factor $\sim 1000$ stricter than used in Governato et al. [2012], and a factor $\sim 100$ stricter than was found to give good convergence in idealized comparisons of dark matter zoom-in simulations in Kim et al. [2014]. Given our very strict default tolerances, this gave well-converged results.

Figure 1 shows visualizations of the gas density (left panel), gas temperature (middle panel) and gas metallicity (right panel) for the Dwarf_early run at $z = 2.3$. All panels show the same thin
3 RESULTS

3.1 Basic Properties at $z = 0$

Table 1 presents some relevant parameters describing the properties of each simulation presented in this work that will allow an immediate comparison with previous simulations and observations of dwarf galaxies.

Of particular interest is the resultant stellar mass in each dwarf. Figure 2 presents the stellar mass - halo mass relation for the four hydrodynamical runs described above (large red points) compared to the most recent estimates for this relation from abundance-matching exercises in the Local Group (Garrison-Kimmel et al. 2014, Brook et al. 2014, black solid and dashed lines respectively).

The known sources of stellar feedback we include, with no adjustment, automatically produces galaxy stellar masses that are consistent with those required to match local galaxy counts. For the halo slice along the $z$-axis centered at the main halo. The signatures of a recent SN episode are clear in all of them.

mass range presented here, this is particularly impressive, as the integrated stellar mass is suppressed by factors of $\sim 1000$ relative to the Universal baryon fraction (upper solid gray line).

The smaller points in Figure 2 show results from previous hydrodynamical simulations of dwarf galaxies (Governato et al. 2010, Sawala et al. 2011, Simpson et al. 2013, Munshi et al. 2013, Shen et al. 2013, Trujillo-Gomez et al. 2015). The open points are those that have reported at least mild flattening of the central dark matter cusp in response to feedback effects. We note that all of those open points are associated with systems that have formed a fair number of stars, with $M_* \gtrsim 7 \times 10^6 M_\odot$ – more massive than the systems of concern for the Too Big to Fail Problem. As we discuss below, one of our runs (Dwarf late, open square) produces a large core while forming significantly fewer stars.

The upper left panel of Figure 3 shows galaxy size, measured as the half-stellar mass radius, versus the total stellar mass of the galaxy for our simulated galaxies (red points). The observed stellar size-mass relation seen for Milky Way satellites (green) and Local Group field dwarfs (yellow) are shown as data points (taken from Wolf et al. 2010, Kirby et al. 2013, 2014, who also compile data from the literature). The upper right panel of Figure 3 shows the total mass within the half-stellar mass radius vs. the half-stellar mass radius, again for our simulated galaxies compared to local galaxies. Finally, the bottom panel shows the stellar-mass metallicity relation. Overall, the simulated galaxies are in good agreement with sizes, metallicities, and total masses seen for galaxies of their stellar mass in the local universe. For example, the Dwarf Late and middle runs show a good agreement with Fornax, Dwarf early’s size and mass are close to Ursa Minor.

Table 1 shows that Dwarf early is much more dark-matter-dominated within 500 pc than Dwarf Late. This also holds when we look at the half-stellar mass radius of each galaxy, instead of at a fixed physical value. Within this radius, Dwarf early has $M_{\text{tot}}/M_* \approx 44$ and $M_{\text{tot}}/M_{\text{baryons}} \approx 11$. By mass, stars are subdominant to gas within the half-light radius by a factor of 2.8 for this dwarf. Within the half-mass stellar radius, Dwarf late has $M_{\text{tot}}/M_* \approx 87$ and $M_{\text{tot}}/M_{\text{baryons}} \approx 5.4$ owing to a large reservoir of gas within the stellar half-mass radius ($M_{\text{gas}} = 16 M_*$, within $r_{1/2}$).

3.2 Star Formation Histories

While the simulated Dwarfs (early, middle, and late) all show similar $z = 0$ stellar masses, they arrived at those final states via different paths. The Ultrafaint run, on the other hand, ends up with a stellar mass some two orders of magnitude smaller than any of the Dwarf runs, though it resides within a halo that is only $\sim 3$ times less massive. In this subsection, we explore these differences by examining the star formation histories in some detail.

In Figure 4 we present the star formation rates (left panel) and the normalized cumulative star formation histories (right panel) of all four high resolution hydro runs. The Ultrafaint simulation (orange line) forms all of its stars before $z \sim 2.5$. The galaxy shuts down at this redshift because of two main effects: 1) the UV background prevents fresh gas accretion after $z \sim 6$ and 2) stellar feedback acts to self-quench the system after the ionizing background radiation as observations throughout the Local Group are not complete below this limit. 

When we do this comparison with observations we are assuming that the half-stellar mass radius is equivalent to the half-light radius.

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Abundance matching results below $\sim 10^9 M_\odot$ stellar mass are extrapolated to lower mass range presented here, this is particularly impressive, as the integrated stellar mass is suppressed by factors of $\sim 1000$ relative to the Universal baryon fraction (upper solid gray line).

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While the simulated Dwarfs (early, middle, and late) all show similar $z = 0$ stellar masses, they arrived at those final states via different paths. The Ultrafaint run, on the other hand, ends up with a stellar mass some two orders of magnitude smaller than any of the Dwarf runs, though it resides within a halo that is only $\sim 3$ times less massive. In this subsection, we explore these differences by examining the star formation histories in some detail.

In Figure 4 we present the star formation rates (left panel) and the normalized cumulative star formation histories (right panel) of all four high resolution hydro runs. The Ultrafaint simulation (orange line) forms all of its stars before $z \sim 2.5$. The galaxy shuts down at this redshift because of two main effects: 1) the UV background prevents fresh gas accretion after $z \sim 6$ and 2) stellar feedback acts to self-quench the system after the ionizing background radiation as observations throughout the Local Group are not complete below this limit.

When we do this comparison with observations we are assuming that the half-stellar mass radius is equivalent to the half-light radius.
This is not unexpected: previous lower-resolution simulations predicted that reionization-induced UV heating is not strong enough to remove all of the gas from dwarf-sized halos (Hoeft et al. 2006). However, these simulations were not able to resolve the star formation histories of these galaxies, so it was not clear if the remaining gas would be able to form stars. As the UV background effectiveness depends on the density of the gas, cold and dense gas is not affected. Moreover, this more efficient star formation period seems crucial in order to match the stellar metallicity ratios observed for low-mass dwarf galaxies (Kirby et al. 2013).

Figure 4 also shows the star formation rates of the three Dwarf runs. Dwarf early forms more than half of its stars prior to \( z = 2.5 \) while Dwarf late maintains a fairly substantial star formation rate down to \( z = 0 \). The Dwarf middle star formation rate history stands just between the two. All of the runs show bursty star formation histories on \( \sim 100 \) Myr timescales.

In all three of the Dwarf runs, the star formation histories show two different phases. At the highest redshifts \( (z > 3) \), total dark halo and stellar masses both grow efficiently (albeit with some offset). This is the “rapid assembly” phase (Wechsler et al. 2002), before/during reionization, in which feedback, while able to eject some gas from the galaxy and provide some overall suppression and variability of the star formation, does not appear to dominate the gas dynamics (the central potential and mass of the halo grow on timescales comparable to the galaxy dynamical time). But from \( z \sim 3 \) onward, halo accretion rates slow down and feedback acts strongly. From this point on, there appears to be a steady-state SFR that can be considered constant with time when averaged over a Gyr scale (a bursty behavior emerges when smaller time bins are used). In this phase, the galaxy is able to cycle new material into a fountain and so maintain equilibrium. This “quasi-equilibrium” SFR scales with the central potential of the galaxy (see Hopkins et al. 2012), as traced by quantities such as the central halo density or \( V_{\text{max}} \) (the maximum circular velocity), not the halo mass.
Table 1. Simulations data. First column stand for the different parameters studied for each simulation. In Columns 2-7 results at $z = 0$ for the simulations presented in this work are shown. Row 2: fixed gravitational softening used for the dark matter particles in physical parsecs. Row 3: baryon particle mass in the high resolution region in solar masses. Row 4: minimum baryonic force softening in parsecs (minimum SPH smoothing lengths are comparable or smaller). Recall that force softenings are adaptive (mass resolution is fixed). Row 5: dark matter particle mass in the high resolution region in solar masses. Row 6: fixed gravitational softening used in simulations (Hydro: Feed-V) (Collisionless) (Hydro: Feed-M) (Collisionless) (Hydro: Feed-M-soft) (Hydro: Feed-V).

$\lambda$ = 0.031 – – – 0.0350 – – –

$\rho_{\text{min}}$ (pc) – 2.54 $\times$ 10$^{-2}$ – 2.54 $\times$ 10$^{-2}$ 2.54 $\times$ 10$^{-2}$ 2.54 $\times$ 10$^{-2}$

1) $\rho_{\text{min}}$ (M$_{\odot}$) 1.5 $\times$ 10$^{3}$ 1.5 $\times$ 10$^{3}$ 35 35 25 28

2) $\rho_{\text{min}}$ (pc) 28 28 35 35 25 28

3) $\rho_{\text{min}}$ (M$_{\odot}$) – 2.54 $\times$ 10$^{-2}$ – 2.54 $\times$ 10$^{-2}$ 2.54 $\times$ 10$^{-2}$ 2.54 $\times$ 10$^{-2}$

4) $\rho_{\text{min}}$ (gas) (pc) – 1.0 – 2.0 – 2.8

5) $\rho_{\text{min}}$ (M$_{\odot}$) 3.2 $\times$ 10$^{9}$ 2.5 $\times$ 10$^{9}$ 9.2 $\times$ 10$^{9}$ 7.6 $\times$ 10$^{9}$ 7.7 $\times$ 10$^{9}$ 7.7 $\times$ 10$^{9}$

6) $V_{\text{max}}$ (km/s) 26 22 37 33 33 32.5

7) $V_{\text{vir}}$ (kpc) 38 35 54 51 51 51

8) $\rho_{\text{min}}$ (gas) (pc) – – – 2.0 – –

9) $f_{\text{star}} \times (\Omega_m/\Omega_\Lambda)$ – 0.024 – 0.093 0.074 0.056

10) $f_{\text{gas}}$ – 0.0049 – 0.018 0.014 0.011

11) $f_{\text{bar}}$ (T/2) (Gyr) – 1.43 – 1.84 – –

12) $\rho_{\text{min}}$ (M$_{\odot}$) – 2.1 $\times$ 10$^{4}$ – 2.8 $\times$ 10$^{6}$ 2.7 $\times$ 10$^{6}$ 2.2 $\times$ 10$^{6}$

13) $\rho_{\text{min}}$ (gas) (pc) – 340 – 1100 830 550

14) $\rho_{\text{min}}$ (gas) (pc) – 10.5 50 – – –

15) $\rho_{\text{min}}$ (gas) (pc) – 0.1 26 – 2.8 – –

16) $\rho_{\text{min}}$ (M$_{\odot}$) 2.2 $\times$ 10$^{7}$ 1.7 $\times$ 10$^{7}$ 3.4 $\times$ 10$^{7}$ 0.75 $\times$ 10$^{7}$ 1.3 $\times$ 10$^{7}$ 1.9 $\times$ 10$^{7}$

17) $\rho_{\text{min}}$ (M$_{\odot}$) 1.6 $\times$ 10$^{7}$ 1.7 $\times$ 10$^{7}$ 2.6 $\times$ 10$^{7}$ 0.43 $\times$ 10$^{7}$ 0.89 $\times$ 10$^{7}$ 1.6 $\times$ 10$^{7}$

18) $\rho_{\text{min}}$ (M$_{\odot}$) – 1.2 $\times$ 10$^{5}$ – 3.2 $\times$ 10$^{5}$ 4.7 $\times$ 10$^{5}$ 2.2 $\times$ 10$^{5}$

19) $\rho_{\text{min}}$ (M$_{\odot}$) – 6.9 $\times$ 10$^{2}$ – 3.1 $\times$ 10$^{5}$ 4.5 $\times$ 10$^{5}$ 1.6 $\times$ 10$^{5}$

20) $\rho_{\text{min}}$ (M$_{\odot}$) – 1.9 $\times$ 10$^{4}$ – 5.4 $\times$ 10$^{4}$ 2.4 $\times$ 10$^{4}$ 6.3 $\times$ 10$^{4}$

21) $\rho_{\text{min}}$ (M$_{\odot}$) – 10$^{4}$ – 10$^{4}$ 10$^{4}$ 10$^{4}$ 10$^{4}$

Figure 4. Left panel: Star formation rates for the hydrodynamical runs presented in this work obtained using two different time bins: 10$^{8}$ yr (full red lines) and 10$^{9}$ yr (dashed black lines). Right panel: Normalized cumulative SFR history for all the hydrodynamical runs presented in this work. Notice the difference of the star formation histories between the three high resolution runs. The vertical grey dashed line marks the reionization redshift assumed in the simulation. Simulated star formation histories are very similar to some observed ones (e.g., Skillman et al. 2014, Weisz et al. 2014). See text for more details.
or virial velocity. The central potential depth increases only weakly over this time as the halo accretes material mostly on its outskirts. This low but constant SFR at low redshift is a key factor in shaping the final matter structure of the dwarf galaxy and will be discussed in detail in the next Section.

Observations of the star formation rate of dwarf galaxies ( Tolstoy et al. 2009; Skillman et al. 2014; Weisz et al. 2014; Brown et al. 2014; Cole et al. 2014) show a relatively high dispersion for a fixed stellar mass, but all the histories of our simulated galaxies seem realistic when compared with these data. In particular, our Ultrafaint galaxy is composed of uniformly old stars, as observed in real ultrafaint dwarf satellites of the Milky Way (Brown et al. 2014), perhaps making them fossils of reionization (Ricotti & Gnedin 2005; Bovill & Ricotti 2011).

Some insight into the extremely low efficiency of star formation in all of these systems can be gained from examining the total baryon fraction vs. time within their associated virial radii. This is shown in Figure 5. Specifically, the virial baryon fraction (baryon mass divided by total mass inside the virial radius) begins declining in the Ultrafaint run from the moment the UV background starts acting to reduce the amount of gas falling into the halo. This allows feedback to be more efficient in expelling the gas out of the halo potential. The Dwarf runs also begin to demonstrate a steady decline in the Ultrafaint run from the moment the UV background starts acting to reduce the amount of gas falling into the halo. This allows feedback to be more efficient in expelling the gas out of the halo potential. The Dwarf runs also begin to demonstrate a steady decline in the Ultrafaint run from the moment the UV background starts acting to reduce the amount of gas falling into the halo. This allows feedback to be more efficient in expelling the gas out of the halo potential.

One intriguing result from Figure 5 is that the overall baryon fraction decreases steadily, without global jumps that are tightly linked to the star formation rate (which varies substantially over ~100 Myr timescales). Instead, the baryons slowly “evaporate” out. This is in contrast with other studies (Sawala et al. 2011; Simpson et al. 2013) that show sharper jumps. However, the lower resolution used by Sawala et al. (2011) could explain why their evolution is less smooth. Simpson et al. (2013) used comparable resolution to this work but studied a lower mass system, 10^9 M☉, which could explain the much more drastic effect due to the UV background in the gas virial fraction that they found.

In the next Section, we study how these differences in the star formation histories affect the matter distribution of the halo.

4 DARK MATTER CONTENT AND STRUCTURE

In Figure 6 we present the dark matter density profiles of the hydrodynamical Ultrafaint (left) and Dwarf (right) runs compared with their equivalent collisionless run at z = 0. The grey bands mark the regions where the simulations are not fully converged according to the criterion of Power et al. (2003) computed for the dark matter only simulation. The Power radius is defined to be the radius where the two-body relaxation time, t_relax, becomes shorter than the age of the universe t₀, where t_relax is determined by the number of particles and the average density of the enclosed region ρ. Specifically, Power et al. found that t_relax < 0.6 t₀ is the best criterion. Elbert et al. (2014) have recently confirmed that this criterion is accurate using zoom simulations of collisionless dwarf halos at similar resolution to those we examine here. The vertical black dotted lines in Figure 6 mark four times the dark matter gravitational softening used in the collisionless runs. We note that while radii larger than the Power radius should not suffer from two-body relaxation, the smallest radius where results in hydrodynamical simulations are converged may be (significantly) larger.

The left panel of Figure 6 shows results for the Ultrafaint simulations. In this case, there is no sign of a decrease in the dark matter density in the hydrodynamical run; in fact the dark matter profile matches perfectly with the collisionless run. In the Dwarf runs (right panel), we observe that all hydrodynamical runs show varying levels of decrease of the inner dark matter density when compared with their equivalent collisionless run. In particular, the Dwarf_late run has produced a fairly large (~1 kpc) constant density core – this is exactly the behavior needed to help alleviate the Too Big to Fail Problem (see, e.g. Elbert et al. 2014; Governato et al. 2015) and that would be required to explain indications of cored profiles in low-mass galaxies in the Local Group. Donato et al. 2009; Salucci et al. 2012; Walker & Peñarrubia 2011; Amorisco et al. 2014; Burkert 2015).

One common way to quantify core formation in halos is to measure the log-slope of the density profile α at 1-2% of the virial radius. The Dwarf halo in the dark-matter only run has α = −1.58, while Dwarf_early, Dwarf_middle, and Dwarf_late have α = −1.39, −0.88, and −0.27, respectively. The late-forming dwarf produces the shallowest profile and the largest core, while the early-forming dwarf produces the densest, cuspiest system.

Over time, in all three dwarf runs, we have observed clear correlations between core formation and star-formation events. However, at early times, as the halos continue to accrete matter and experience central mergers, the cusps regrow regularly. During the early, rapid accretion phase, evolution in the density structure is fairly stochastic, with cores forming in response to blow-out events, and then becoming erased as cusps reform in response to mergers. Figure 7 illustrates the formation of the dark matter core using two time steps. Shown are the dark matter density profiles of the Dwarf runs at z = 3.9 (left) and z = 2.2 (right). At z = 3.9, very lit-
Figure 6. Left: The dark matter density profile at $z = 0$ for the collisionless (black line) and hydrodynamical (red line) runs of the $3 \times 10^9 M_\odot$ halo. The “collisionless” line has been converted to the effective dark matter density by accounting for the fact that a fraction $\Omega_b/\Omega_m$ of each particle is assumed to be baryonic in these runs. The bottom panel shows the ratio between the two profiles. Right: The same for the Dwarf halo runs, where each hydrodynamical run is marked by a different style of red line. Grey shaded area marks the region below the convergence radius defined using $\Omega_b/\Omega_m$ criteria for the collisionless run. The vertical black dotted line marks four times the dark matter gravitational softening used in the collisionless runs. Note that the Dwarf_late run has produced a large ($\sim 1$ kpc) constant-density core, while the Dwarf_early has a dark matter profile that is very similar to the dissipationless simulation for radii that are well converged. The dark matter in the hydrodynamic Ultrafaint run is identical to that of the dissipationless case.

Figure 7. Time variation in density profiles. The dark matter density profile at $z = 3.9$ (left figure) and $z = 2.2$ (right figure) for the collisionless (black) and hydrodynamical (red lines) runs of the $1 \times 10^9 M_\odot$ halo. Bottom panel shows the ratio between the two profiles. The vertical black dotted line marks four times the dark matter gravitational softening used in the collisionless runs. Grey shaded area marks the region below the convergence radius defined using $\Omega_b/\Omega_m$ criteria for the collisionless run. Note that, at $z = 2.2$, Dwarf_late has a higher central density than Dwarf_early. Late-time star formation in Dwarf_late serves to reduce the dark matter halo’s density in the center by a factor of $\sim 5$ by $z = 0$ (see right panel of Fig. 6), while Dwarf_early has little star formation subsequent to $z = 2.2$. Its density profile remains essentially unchanged from $z = 2.2$ to $z = 0$.

tle star formation has occurred and the halo is experiencing very rapid growth and we see no decrease in core dark matter density compared to the collisionless run. However, at $z = 2.2$, there are some signs of a decrease in the central dark matter density in the hydro runs. Interestingly, Dwarf_late – which has the largest core at $z = 0$ – has the smallest core profile at $z = 2.2$. Dwarf_early shows almost the opposite trend, owing to the fact that it has had more star formation by $z = 2.2$ than the later forming dwarf.

To further explore the evolution of the dark matter density with time, Figure 8 compares the cumulative star formation history (dashed curves, normalized to unity at the present day) and the mass interior to radii of 0.3, 0.75, and 2 kpc relative to the collisionless run as a function of time for Dwarf_late (left panel) and Dwarf_early (right panel). In both cases, the early phases of galaxy formation ($z \geq 3$) result in fluctuations in the inner mass profiles of these galaxies (Davis et al. 2014). After $z = 3$, when the dark matter assembly of each halo is essentially complete, Dwarf_early forms only a relatively small amount of stars. This results in at most a slight reduction in the inner dark matter mass (right panel). Dwarf_late, however, forms more than 50% of its stellar mass after $z = 2$. Most of the density reduction also occurs after this phase, pointing to a link between the final densities of these objects and their late-time star formation histories. This is consistent with Laorte & Peñarrubia (2015), who found that cusps can regrow after early core formation.

Figure 9 further illustrates the correlation between star formation history and core formation, now with the early and late runs on the same plot, and using dimensional star formation histories rather...
than normalized ones. Specifically, the cumulative star formation histories of the Dwarf_early (green dash) and Dwarf_late (red dash) runs are shown along with the evolution of the ratio of dark matter enclosed within 0.3 kpc for the hydrodynamic compared to the dark-matter only runs (solid lines). It is clear that a higher star formation rate at late times (from $z \approx 2$) produces a bigger decrease in the central dark matter density. Notice that although this difference in the star formation rate below $z = 2$ produces very different cores, the difference in the total amount of stars at $z = 0$ is minimal (see Figures 2 and Table I). In concordance with this picture, lower resolution runs, which have slightly higher star formation rates at low redshift than their high resolution counterparts, show bigger cores in their dark matter distribution (see Appendix B).

It is likely that the relationship between when the stars form and core formation is most important at this critical stellar mass / halo mass scale ($M_* \sim 2 - 3 \times 10^8 M_\odot$ within $\sim 10^{10} M_\odot$ halos). Previous simulation efforts (Pontzen & Governato 2012; Di Cintio et al. 2014) have found that dark matter cores are usually not created in galaxies with so few stars in halos below $\sim 10^{10} M_\odot$. We suggest that at this critical mass scale, where the energy from feedback sources is just at the edge of that required for core formation, small variations in star formation histories can significantly alter the result. Indeed, in our general analysis of the dark matter properties in all FIRE runs, we find a similar transition around $10^{10} M_\odot$ (Chan et al., in preparation).

### 4.1 Energy considerations

Recently, there has been some discussion in the literature about the energy requirements for the formation of a core in a dwarf galaxy halo (see, for example, Peharrubia et al. 2012; Garrison-Kimmel et al. 2013; Teyssier et al. 2013 and references therein) — specifically, how many stars are required for there to be enough energy available to create a core? At first comparison, the fact that the Dwarf_late simulation was able to produce a sizable core with so few stars appears to be in contradiction to the results of Garrison-Kimmel et al. (2013), who suggested that cores this large are not energetically possible. However, the host halo considered in Garrison-Kimmel et al. (2013) is more concentrated than the one we consider here. In order to explicitly check whether our results make sense energetically we aim to compare the energy released in supernovae in our simulations to the difference in dark matter gravitational energy potential of the dwarf hydro runs and its collisionless version.

The gravitational potential energy is defined as:

$$U = -4\pi G \int_{r_{\text{min}}}^{r_{\text{max}}} r M(r)\rho(r)dr$$

(1)

We computed this value numerically directly from the simulation data. We considered $r_{\text{min}} = 0$ (using $r_{\text{min}} = r_{\text{dm}}$ or $r_{\text{min}} = r_{\text{min},\text{gas}}$ gives very similar results) and $r_{\text{max}} = 2$ kpc. We used this maximum radius because we are interested in the energy necessary to decrease the inner part of the density profile and from this point the dark matter profiles match almost exactly (see Figure 6). More importantly, at larger radii differences between the gravitational energy potential can be significant just due to the exact position of the substructure between the collisionless and the hydrodynamic runs. Therefore this definition of potential energy for each run sets a lower energy limit on the amount of energy necessary to create a specific dark matter decrease in the inner part of a halo. We define $\Delta U_{\text{dm}}$ as the difference between the potential energy of the hydrodynamical run and the potential energy of the collisionless run.

In order to obtain an estimate of the energy available from feedback we have considered the energy available from SNe using the parameters from our simulations: $E_{\text{tot}} = (M_{\text{star}}/m) f E_{\text{sn}}$, where $E_{\text{sn}} = 1 \times 10^{51}$ erg is the energy of one supernova, $f = 0.0037$ is the fraction of stars more massive than $8 M_\odot$ for a Kroupa (2002) IMF, and $m = 0.4 M_\odot$ is the mean stellar mass. The stellar mass of the central galaxy at $z = 0$ is between $\sim 2.3 - 2.8 \times 10^9 M_\odot$ however from Figure 8 we can see that the core starts to form below $z \approx 2$, therefore we have also considered the stellar mass produced since this time until $z = 0$. We are considering just supernova energy but in principle, just taking into account the energy, the contribution from photoionization and radiative
Figure 9. The cumulative star formation history (dashed lines) and the dark matter mass ratio between the hydrodynamical run and the collisionless run at 0.3 kpc (full lines) for the early and late forming Dwarf runs.

Figure 10. Energy considerations in the formation of the dark matter cores in a $10^{10} M_\odot$ halo. The x-axis show the total stellar mass for each of the dwarf runs (green symbols) and the amount of stellar mass formed between redshift $z = 2$ and $z = 0$ (red symbols). The upper axis show the energy expelled by SN from this stellar population. The y-axis show the difference in potential energy between the hydrodynamical run and the collisionless run. The right y-axis show the size of the core created due to this difference of energy. See text for details.

5 SUMMARY AND CONCLUSIONS

We have performed several high-resolution zoom-in hydrodynamical simulations of an ultrafaint galaxy halo ($3 \times 10^9 M_\odot$) and a dwarf galaxy halo ($1 \times 10^{10} M_\odot$). Our simulations include all major sources of stellar feedback, implemented directly from stellar evolution calculations. Without parameter tuning, the code reproduces a relation between galaxy stellar mass and halo mass that is consistent with observations. Moreover, we find that global properties of these simulated halos – including their characteristic sizes, metallicities and gas contents – are well-matched to observed galaxies of similar stellar mass. These global properties describing the simulated dwarfs are robust to changes in force and mass resolution. Furthermore, the feedback models and the outflows they generate are inherently multi-phase, matching observations. The predictive nature of our galaxy formation model is particularly important, as the model does not contain ad hoc numerical solutions adopted by other models, e.g. cooling shut-offs or prescribed wind properties, that contain adjustable parameters. The mass scale of our simulated dwarfs – $M_\star \sim 2 \times 10^6 M_\odot$ – is particularly relevant because previous models able to generate cores have usually formed almost an order of magnitude more stars in such halos ($M_{vir} = 10^{10} M_\odot$). Such galaxies are too massive in terms of the number of stars given their halo mass and therefore cannot be typical, given observed galaxy counts around the Milky Way and generic predictions from $\Lambda$CDM simulations (Garrison-Kimmel et al. 2014; Brook et al. 2014).

Our models show a slow but continuous decrease of the baryonic mass inside the virial radius after $z \sim 6$. The UV background, in concert with star formation feedback, plays a fundamental role in regulating star formation in low-mass systems and appears to be the driving factor in suppressing gas accretion in our ultrafaint run. However, for the halo masses studied in this work, the UV background does not shut down star formation immediately because it is not efficient in heating the high density gas in the center of these halos. The simulated ultra-faint ($M_{vir} = 3 \times 10^9 M_\odot$) continues forming stars for $\sim 2$ Gyr following reionization (at which time it runs out of cold gas; such an object would be a counterpart in the field to known ultra-faint satellites of the Milky Way), while the more massive dwarfs continue to form stars to $z = 0$. This may indicate a transition from lower-mass objects that are incapable of acquiring cold gas after reionization to dwarfs at this mass scale that can continue to accrete fuel for subsequent star formation.

We have also studied, in detail, the dark matter distribution of...

8 We define the size of the core at the radius where the mass ratio between the hydrodynamical over the collisionless runs is 0.9 (see Figure 9).
these halos. The simulated dwarfs ($M_\star \sim 2 \times 10^6 M_\odot$) have a variety of density profiles, ranging from a small modification of the equivalent dark-matter-only simulation to a substantial (kpc-scale) core. The simulated ultra-faint galaxy ($M_\star \sim 2 \times 10^4 M_\odot$) does not form enough stars to modify its dark matter halo at all, providing further support to the idea that there is a critical mass below which core formation caused by stellar feedback is energetically impossible (see, e.g., Governato et al. 2012 [Garrison-Kimmel et al. 2013; Madau et al. 2014]). Our results indicate that stellar mass is not the only parameter in core creation, however. The creation of dark matter cores is linked with late-time star formation properties, as only the system with significant late-time star formation forms a sizeable core. The galaxy that forms most of its stars at early time is able to create a core temporarily, but subsequent dark matter accretion and mergers and the lack of strong star formation erase this core, leaving a cuspy profile. The difference in density at 300 pc between these two extreme cases is a factor of $\approx 4$. A related point is that the formation of stable dark matter cores is a continuous process, not instantaneous, and that the creation of significant cores in dwarf galaxies does not appear to be an inevitable outcome in models with bursty star formation histories.

A question that remains unclear is whether these cored systems can avoid regenerating a density cusp once they merge with smaller, cuspy, haloes (Laporte & Penarrubia 2015). The late-time merger history of dwarfs can vary significantly (e.g., Deason et al. 2014), meaning it is imperative to simulate a statistical sample of halos at a given mass to fully understand trends in core formation or cusp regrowth (Fitts et al., in preparation). It will also be imperative to test this scenario at different halo masses (Chan et al., in preparation), as many models predict a core formation efficiency that varies with the halo mass (e.g., Di Cintio et al. 2014). We have not considered the effects stripping from ram pressure and tides, that may be important for some Milky Way subhalos (Read et al. 2006; Zolotov et al. 2012; Brooks & Zolotov 2014). However, the central prediction coming from our simulations is observationally testable: the presence of cores in galaxies with stellar masses of $\sim 10^8 - 10^9 M_\odot$ requires substantial late time star formation.

ACKNOWLEDGMENTS

This work used computational resources granted by NASA Advanced Supercomputing (NAS) Division, NASA Center for Climate Simulation, Teragrid and by the Extreme Science and Engineering Discovery Environment (XSEDE), which is supported by National Science Foundation grant number OCI-1053575. JO and JSB were supported by NSF grant AST-1009999 and NASA grant NNX09AG01G. JO thanks the financial support of the Fulbright/MICINN Program. JO also thanks the pynbody team for making this software publicly available. DK was supported by a Hellman Fellowship and NSF grant AST-1412153. CAFG was supported by NSF through grant AST-1412836, by NASA through grant NNX15AB22G, and by Northwestern University funds.

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APPENDIX A: DARK MATTER PROPERTIES AND EVOLUTION IN THE COLLISIONLESS RUN

To choose the specific dwarf galaxy halos to re-simulate we rely on collisionless simulations. We have taken into account two things: first we wanted them to be cheap in terms of cpu cost and second we wanted them to be representative of the dwarf galaxy halo population. We point to Oñorbe et al. (2014) for a full description of the method. Here we just want to show how the properties of our selected halos compare with a realistic sample of dwarf galaxy halos. To generate this sample we run a $L_{box} = 35$ Mpc collisionless simulation ($512^3$ simulations). Figure A1 show the spin ($\lambda$), concentration ($V_{max}/V_{vir}$), halo formation time ($t_{50}$) and virial mass distributions for all the main halos in this simulation (so excluding subhalos) with virial masses between $3 \times 10^9 M_\odot$ and $3 \times 10^{10} M_\odot$. The mass bin sample includes around $\sim 15000$ halos. Halo spin parameters were calculated using Bullock et al. (2001) definition. In order to estimate the time of formation for each halo, we followed the approach described in Wechsler et al. (2002). We fit the halo accretion histories obtained from the merger trees to an exponential form that depends on one parameter. The halo formation time $t_{50}$ is calculated at the time when the halo reached half of its total mass. The chosen parameters for our ultrafaint and dwarf initial conditions are plotted as a white triangle and a white square respectively. The exact values can be found in Table 1. This Figure show that the re-simulated halos picked from our $L_{box} = 7$ Mpc box have very typical values of spin and concentration. The reason why our formation time is a bit lower than the standard value is a combination of three factors. First we preferred to avoid systems with late major mergers events which also helps to reduce the cpu cost of the simulation Oñorbe et al. (2014). The dwarf halo sample from a smaller box is biased towards smaller formation times so there were a smaller range of possible halos to pick which fulfill all our desired criteria. Finally, the circular velocity profile of the Dwarf_dm simulation, which can be found in [Bullock et al. (2014)] (left panel), shows that the halo has too high density to match the circular velocity observations of Local Field dwarf galaxies. This makes it a suitable candidate to study the Too Big To Fail problem.

Figure A2 shows the evolution of the dark matter mass profile for the Dwarf collisionless simulation. Each line shows the amount of dark matter mass contained inside a fixed physical radius. At
high redshift the halo shows a characteristic fast halo mass increase followed by a very shallow evolution at high redshift. Notice how the inner parts of the profile takes a bit more time to settle down. Below redshift \( z \sim 2.5 \) the inner part of the halo does not show any significant perturbation as there is no significant accretion or merger (Diemand et al. 2007; Diemer et al. 2013).

**APPENDIX B: CONVERGENCE**

In this Section we present a convergence study that we have performed for the Dwarf galaxy halo. We have run a lower resolution version of all the Dwarf hydrodynamical runs discussed above. The only difference between the high and low resolution runs are the different particle masses and softenings used in the runs. The star formation density threshold, \( n_{sf} \), is also slightly different between the runs, \( 10 \text{ cm}^{-3} \) for low res and \( 100 \text{ cm}^{-3} \) for high res. All other code and physical parameters are exactly the same as for the high resolution runs. In Table [B1] all the relevant parameters of these lower resolution runs can be found.

The different panels of Figure [B1] illustrate the differences between the runs. The main difference that we found is that the low resolution runs have slightly higher stellar masses (upper left panel of Figure [B1]). This can be understood by looking at the SFR histories (upper right panel in Figure [B1] blue lines stand for low resolution runs and red lines for the high resolution ones). The main difference observed between resolutions is the steeper slope of the cumulative star formation history at lower redshift. This produces higher stellar masses at \( z = 0 \) for the lower resolution runs. We think that this is because the minimum amount of star formation that is possible is set by the gas particle resolution. Therefore the minimum amount of star formation is higher in the lower resolution runs. It is remarkable that all galaxy trends with size and metallicity hold regarding of resolution, so the galaxies seems just move along these relations (lower left panel of Figure [B1]). We have also re-run our dwarf galaxy low resolution initial conditions using exactly the same code to check for pure stochastic differences. The scatter found in all the properties studied in this paper was similar to the one that we found when we change the feedback implementation and/or the softening values. These authors suspect that these differences will decrease at higher resolution, though higher resolution runs will certainly be required in order to test this conjecture.

Finally, concerning the core formation and energy considerations, low resolution runs also form a core which seems to be directly connected with its star formation rate at low redshifts (\( z \lesssim 2 \)). In general these cores are more prominent than their high resolution counterparts due to the higher star formation rate discussed above. Remarkably when we plot the energy requirements to form these cores versus the amount of energy obtained from supernova feedback below \( z = 2 \) (lower right panel of Figure [B1]), they lie in the same range of efficiencies as their high resolution counterparts.

Although it is not possible to claim full convergence for our high resolution runs from these results, we think that they are at least quite encouraging and definitely an improvement from other
Figure B1. Convergence tests. High (red) and low (blue) resolution simulations. Upper left: The stellar mass - halo mass relation. Upper right: Cumulative star formation history. Lower left: Metallicity versus stellar mass. Lower right: Energy considerations in the formation of the dark matter cores in a $10^{10} M_\odot$ halo. See text for details.

approaches in which parameters of the sub-grid physics must be tuned at each resolution.
Table B1. Simulations data for the low resolution convergence tests. First column stand for the different parameters studied for each simulation. In Columns 2-9 results for the simulations presented in this work are shown. Row 1: dark matter particle mass in the high resolution region in solar masses. Row 2: fixed gravitational softening used for the dark matter particles in physical parsecs. Row 3: baryon particle mass in the high resolution region in solar masses. Row 4: minimum baryonic force softening in parsecs (minimum SPH smoothing lengths are comparable or smaller). Recall, force softenings are adaptive (mass resolution is fixed). Row 5: virial mass in solar masses defined at the overdensity at which the spherical top hat model predicts virialization (Bryan & Norman [1995]). Row 6: maximum circular velocity in km/s. Row 7: virial radius in kiloparsecs. Row 8: virial baryon fraction, i.e., baryon mass inside the virial radius over the virial mass. Row 9: virial gas fraction, i.e., gas mass inside the virial radius over the virial mass. Row 10: virial stellar fraction, i.e., stellar mass inside the virial radius over the virial mass. Row 11: stellar mass in solar masses. This is the stellar mass of the central galaxy. Row 12: effective stellar mass over the virial mass. Row 13: stellar gas fraction, i.e., stellar mass in solar masses defined at the overdensity at which the spherical top hat model predicts virialization (Bryan & Norman [1995]). Row 14: total mass inside 500 parsec in solar masses. Row 15: dark matter mass inside 500 parsec in solar masses. Row 16: baryon mass inside 500 parsec in solar masses. Row 17: gas mass inside 500 parsec in solar masses. Row 18: stellar mass inside 500 parsec in solar masses.

| Parameter | Dwarf$_{dm,Lr}$ (Collisionless) | Dwarf$_{late,Lr}$ (Hydro: Feed-M) | Dwarf$_{middle,Lr}$ (Hydro: Feed-M-soft) | Dwarf$_{early,Lr}$ (Hydro: Feed-V) |
|-----------|------------------|-------------------|------------------|------------------|
| 1) $m_{dm}^{15}$ ($M_{\odot}$) | $1.21 \times 10^4$ | $1.01 \times 10^4$ | $1.01 \times 10^4$ | $1.01 \times 10^4$ |
| 2) $\epsilon_{dm}$ (pc) | 35 | 35 | 35 | 35 |
| 3) $m_{bar}^{15}$ ($M_{\odot}$) | – | $2.04 \times 10^3$ | $2.04 \times 10^3$ | $2.04 \times 10^3$ |
| 4) $\epsilon_{gas}^{15}$ (pc) | – | 2.0 | 35 | 2.0 |
| 5) $M_{vir}$ ($M_{\odot}$) | $9.48 \times 10^9$ | $7.60 \times 10^9$ | $7.60 \times 10^9$ | $7.46 \times 10^9$ |
| 6) $V_{max}$ (km/s) | 37.31 | 32.79 | 32.79 | 33.56 |
| 7) $r_{vir}$ (kpc) | 54.99 | 51.08 | 51.08 | 50.77 |
| 8) $f_{bar}$ | – | 0.0166 | 0.0171 | 0.0137 |
| 9) $f_{gas}$ | – | 0.0165 | 0.0165 | 0.0121 |
| 10) $f_{\ast}$ | – | 0.0006 | 0.0006 | 0.0016 |
| 11) $M_{\ast}$ ($M_{\odot}$) | – | $4.1 \times 10^6$ | $4.2 \times 10^6$ | $1.0 \times 10^7$ |
| 12) $r_{1/2}$ (kpc) | – | 0.783 | 0.881 | 1.311 |
| 13) $[Fe/H]$ | – | $-1.493$ | $-1.468$ | $-1.450$ |
| 14) $M_{500}^{dm}$ ($M_{\odot}$) | $3.212 \times 10^7$ | $1.285 \times 10^7$ | $1.014 \times 10^7$ | $4.088 \times 10^6$ |
| 15) $M_{500}^{bar}$ ($M_{\odot}$) | $2.414 \times 10^7$ | $7.366 \times 10^6$ | $7.132 \times 10^6$ | $3.703 \times 10^6$ |
| 16) $M_{500}^{gas}$ ($M_{\odot}$) | – | $5.483 \times 10^6$ | $3.002 \times 10^6$ | $3.861 \times 10^5$ |
| 17) $M_{500}^{light}$ ($M_{\odot}$) | – | $5.083 \times 10^6$ | $2.635 \times 10^6$ | 0.0 |
| 18) $M_{500}^{stellar}$ ($M_{\odot}$) | – | $4.004 \times 10^5$ | $3.677 \times 10^5$ | $3.861 \times 10^5$ |