Research Article

Wagner-Vengrenovich Distribution

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The process of coarsening of nanoclusters or nanocrystals (NCs) is investigated for the case when cluster growth (dissolution) is governed simultaneously by both diffusion along dislocation pipes and the rate of formation of chemical connections (chemical reaction) at clusters surface, namely, Wagner’s growing mechanism. For that, the total flow of atoms to (from) a cluster is represented by two parts, namely, diffusion part and the Wagner (kinetic) one. The dependence of the rate of growth of NC on the ratio of the parts of the total flow has been determined as well as the NC’s size distribution function referred to as the Wagner-Vengrenovich distribution. Computed distribution is compared with experimentally obtained histograms.

1. Introduction

Ostwald’s ripening (OR) is the final stage of formation of a new phase as a result of phase transformation, such as decay of oversaturated solid solutions. Nanoclusters or nanocrystals (NCs) of new phase having different sizes interact through the Gibbs-Thomson effect that results in dissolution of small NC and growth of large ones. Diffusion growth of NC under matrix of volume diffusion ($ls$-mechanism) has been firstly studied by Lifshitz and Slyozov [1, 2]. Wagner has showed later [3] that beside diffusion mechanism, another mechanism of NC growth is possible, which is governed by the rate of formation of chemical connections (chemical reaction) at NC surface ($w$-mechanism). The theory developed in the cited papers is referred to as the LSW theory. Practical verification of this theory shows that in many cases, it is proper for the description of experimental data on temporal behavior of the mean NC size and the NC size the distribution function, while in other cases the LSW theory must be refined.

In this connection, NC growth is considered in papers [4, 5] as a result of combined action of two growing mechanisms, diffusion ($ls$) and Wagner’s ($w$) ones. In the framework of the modified LSW theory and taking into account both mechanisms of growing ($ls$ and $w$), we can obtain a size distribution in the form of the generalized Lifschitz-Slyozov-Wagner distribution [4]. This distribution can refer to a much wider range of the experimental histograms than each of the Lifschitz-Slyozov (LS) and Wagner’s ($W$) distributions separately.

The products of nanotechnologies [6–8] become new objects of applying the LSW theory. As sizes become 100 nm and less [9], the characteristics of both separate NCs and of the system as a whole change cardinally that provides practically useful properties. The OR is among probable factors destabilizing microstructure and properties of nanocluster systems. Semiconductor heterosystems with quantum dots (QDs) obtained by electron-beam epitaxy technique [10–16] in the Stranski-Krastanov regime [17] as well as arrays of QDs synthesized from liquid matter by chemical and other techniques [18–25] are examples of such nanocluster systems.

As it has been mentioned above, the generalized LSW distribution has been obtained by combination of the diffusion ($ls$) and Wagner’s ($w$) mechanisms of NC growth. However, in presence of a matrix of free dislocations interacting with elastic fields of NCs or in presence of NCs located at dislocation network, just dislocation diffusion ($v$-mechanism of NC growth) predominates rather than matrix one. Peculiarities of the Ostwald’s ripening under diffusion along dislocation pipes have been considered supra [26–30].
The purpose of this paper consists in finding out the size distribution function and temporal dependences of NC mean size for the case when NC growth is governed simultaneously by both mechanisms, namely, dislocation diffusion \((v)\) and the rate of formation of chemical connections (chemical reaction) at cluster surface \((w)\). Computations are carried out within the framework of the modified LSW theory \([4]\), using the technique introduced in paper \([31]\).

### 2. Theoretical Part

As NC growth is governed by two mechanisms \((v\) and \(w)\) simultaneously, the total flow of atoms to (from) NC consists of two parts \([4]\)

\[ j = j_d + j_i, \quad (1) \]

where \(j_d\) is the diffusion part of flow that equals the number of atoms reaching cluster surface in unit time through dislocation diffusion and \(j_i\) is the Wagner’s part of flow that equals the number of atoms involved in forming chemical connections at cluster surface in unit time.

To determine the size distribution function, \(f(r, t)\), let us use the continuity equation

\[ \frac{\partial f(r, t)}{\partial t} + \frac{\partial}{\partial r} \left[ f(r, t) \cdot \dot{r} \right] = 0, \quad (2) \]

where \(\dot{r} \equiv dr/dt\) is the rate of growth of cluster with radius \(r\), which is determined from the following condition:

\[ \frac{d}{dt} \left( \frac{4}{3} \pi r^3 \right) = j v_m, \quad (3) \]

where \(j\) is determined by \((1)\).

In accordance with \([27]\), the diffusion part of a flow equals

\[ j_d = D_2 Z q \frac{(C) - C_r}{r}, \quad (4) \]

where \(D_2\) is the diffusion coefficient along dislocations, \(Z\) is the number of dislocation lines crossing a cluster \((Z = \text{const})\), \(q\) is the cross-section of dislocation pipe, \((C)\) is the mean concentration of diffusing atoms into solution, \(C_r = C_{co} \exp(2\sigma v_m/rkT) \approx C_{co}(1 + 2\sigma v_m/rkT)\) is that concentration of atoms of solved matter at the boundary of a cluster of radius \(r\), \(C_{co}\) is that equilibrium concentration for the specified temperature \(T\), and \(v_m\) is that volume of an atom of solved matter.

Wagner’s (kinetic) part of a flow equals \([3]\):

\[ j_i = 4\pi r^2 \beta (\langle C \rangle - C_r), \quad (5) \]

where \(\beta\) is the kinetic coefficient.

Knowing \(j_d\) and \(j_i\), one finds out the rate of cluster growth from \((3)\). Consider the following:

\[ \frac{dr}{dt} = \frac{1}{4\pi r^2} \left[ D_2 Z q \frac{(C) - C_r}{r} + 4\pi r^2 \beta (\langle C \rangle - C_r) \right], \quad (6) \]

where \(\langle C \rangle - C_r = (2\sigma v_m/kT)/(1/r_k - 1/r)\), \(r_k\) is the critical radius that, within the LSW theory approximation, assumes to be equal to the mean radius, \(\langle r \rangle\).

To determine the analytical form of the size distribution function of clusters with peculiarities intrinsic in Wagner’s \((W)\) distribution \([3]\) and Vengrenovich’s \((V)\) distribution \([27]\), one must express the rate of growth \((6)\) as the ratio of flows \(j_d\) and \(j_i\)

\[ \frac{j_d}{j_i} = \frac{x}{1-x}, \quad (7) \]

where \(x\) is the part of flow \(j_d\) in the total flow \(j : x = j_d/j\) and \((1-x)\) is the part of flow \(j_i\) in the total flow \(j : 1-x = j_i/j\). Taking into account that \((4)\) and \((5)\) for flows are valid for NCs of arbitrary radius \(r\), including NCs of the maximal size \(r_g\) \([4,5]\), one can rewrite \((6)\) in the form

\[ \frac{dr}{dt} = A^* \left( \frac{x}{1-x} \right) \left( \frac{r}{r_k} - 1 \right), \quad (8) \]

where \(A^* = 2\sigma^2 n C_{co} \beta/kt\), \(u = r/r_g\), or in the form

\[ \frac{dr}{dt} = B^* \left( 1 - \frac{x}{x} \right) \left( \frac{r}{r_k} - 1 \right), \quad (9) \]

where \(B^* = (2\sigma^2 n C_{co} Z q D_d)/nkT\).

Equation \((8)\) corresponds to the rate of growth of NCs that is determined by the kinetic flow \(j_i\), namely, by the rate of formation of chemical connections, with the share contribution \((1-x)\) of the diffuse flow \((x < 1)\), and the rate of growth \((9)\) is determined by the diffuse flow \(j_d\) with the share contribution \(x\) of the kinetic flow \((x > 0)\).

From \((8)\) or \((9)\), for the rate of growth, one can determine the ratio \(r_g/r_k\) that in terms of paper \([1]\) corresponds to the locking point magnitude, \(u_0\) \(\left( u_0 = r_g/r_k \right)\). Knowing \(u_0\) enables to integrate \((8)\) and \((9)\) and to find out temporal dependences for \(r_g\) and \(r_k\), as well as to separate the variables in the continuity equation \((2)\) and to find out the analytical form of the size distribution function. In accordance with \([31]\), the ratio \(r_g/r_k\) \((u_0)\) can be found out from the dependence of the specific rate of growth \(\dot{r}/r\) on \(r\) shown schematically in Figure 1. Derivative equals zero at the maximum of this function

\[ \frac{d}{dr} \left( \frac{\dot{r}}{r} \right) = 0. \quad (10) \]

From \((10)\), one obtains

\[ \frac{r_g}{r_k} = \frac{2 + 3x}{1 + 3x}. \quad (11) \]

Assuming \(r = r_g (u = 1)\) in \((8)\) and replacing the ratio \(r_g/r_k\) by its magnitude from \((11)\), one obtains by integration

\[ \frac{r_g^2}{(1-x)} = \frac{2A^* (1+3x)}{(1-x)} \frac{1}{(2+3x)^2} t. \quad (12) \]

Equation \((12)\) determines the temporal dependences for the maximal radius of NCs, \(r_g\), and the critical one, \(r_k\), when the Wagner’s mechanism of growth predominates. The limits of changing parameter \(x\) can be determined from comparison
of experimental and theoretical data, for example, for size distribution function, which equals in our case \(0 \leq x \leq 0,3\), approximately.

For \(x = 0\), growth of NCs is completely controlled by the rate of formation of chemical connections (the \(w\)-mechanism) [3]

\[
r_g^2 = 2A^*t, \quad r_k^2 = \frac{1}{2}A^*t, \quad \frac{r_g}{r_k} = 2. \tag{13}
\]

Similarly, one obtains from (9)

\[
r_g^5 = \frac{5B^*(1 + 3x)^4}{x(1 + 3x)^4}, \quad r_k^5 = \frac{5B^*(1 + 3x)^4}{x(2 + 3x)^5} - t. \tag{14}
\]

Equation (14) corresponds to the temporal dependences of changing \(r_g\) and \(r_k\), when diffusion along dislocation pipes predominates in the growth of NCs. For that, the parameter \(x\) changes within interval \(0,7 \leq x \leq 1\), approximately.

For \(x = 1\), growth of NCs is completely controlled by the diffusion of solved atoms along dislocation pipes (the \(v\)-mechanism) [26, 27]:

\[
r_g^5 = \frac{5B^*}{x(1 + 3x)^4}, \quad r_k^5 = \frac{5B^*(1 + 3x)^4}{x(2 + 3x)^5}, \tag{15}
\]

In accordance with [26], the total change of NCs’ volume, \(\Delta V_x\), consists from \(\Delta V_d\), that is, the change caused by the dislocation flux, \(j_d\), and \(\Delta V_k\) caused by the kinetic flux, \(j_k\),

\[
\Delta V_x = \Delta V_d + \Delta V_k, \tag{16}
\]

or

\[
4\pi r_k^3 = \frac{4}{3}\pi r_k^3 + \frac{4}{3}\pi r_k^3, \tag{17}
\]

where for the sake of simplicity, time reading is made from zero: \(t = t_0 = 0\); \(r_k^3(t_0) = 0\); \(r_g^3(t_0) = 0\); \(r_k^3(t_0) = 0\). Taking into account (12) and (14), one obtains from (17)

\[
r_k^3 = \left[ f_1(x) t^{3/5} + f_2(x) t^{1/2} \right]^{1/3}, \tag{18}
\]

where \(f_1(x) = 5B^*(1 + 3x)^4/(x(2 + 3x)^5), f_2(x) = 2A^*(1 + 3x)/(1 - x)(2 + 3x)^2\), and the limits of changing total radius of NCs \(x\) are \(0,3 \leq x \leq 0,7\), approximately.

In accordance with [31], the size distribution function of NCs is found out as the product of two functions

\[
f(r, t) = \varphi \left( \frac{r_g}{r_k} \right) g^*(u), \tag{19}
\]

where \(r_g = \psi(t)\).

By substitution (19) into the mass conservation law for disperse phase (NCs),

\[
M = \frac{4}{3} \pi \rho \int_{0}^{r_g} r^3 f(r, t) dr, \tag{20}
\]

one obtains

\[
\varphi \left( \frac{r_g}{r_k} \right) = \frac{Q}{r_g}, \tag{21}
\]

where \(Q = 3M/4\pi \rho \int_{0}^{1} u^3 g^*(u) du\).

Taking into account (21), one can write the size distribution function in the form

\[
f(r, t) = \frac{1}{r_g} g(u), \tag{22}
\]

where

\[
g(u) = Q g^*(u), \tag{23}
\]

and \(g(u)\) is the required distribution function on relative sizes of NCs, called by us the Wagner-Vengrenovich (WV) distribution function, as the distributions corresponding to each of the mechanisms, \(w\) and \(v\), separately have been early obtained by Wagner (W) [3] and Vengrenovich (V) [27].

For determining \(g^*(u)\), let us use the continuity equation (2) substituting in this equation, instead of \(f(r, t)\) and \(r\), their magnitudes from (19) and (8) (or (9)). By transition in (2), from differentiation on \(r\) and \(t\) to differentiation on \(u\) [31], variables are separated

\[
\frac{dg^*(u)}{g^*(u)} = -\frac{4u v g^* + v - u (dv/du)}{u^3 v_g - v u} du, \tag{24}
\]

where one takes into account that \(v = \dot{r}r/A^*, v_g = \dot{r}_g r/A^*\), \(du/dr = 1/r_g\), and \(du/dr_g = -u/r_g\).

Finding out \(v, g^*, v_g\) and \(dv/du\) from (8), one can rewrite (24) in the form

\[
\frac{dg^*(u)}{g^*(u)} = -\frac{4u v^3 + u^3 \left(3x^2 - 2x - 1\right) + ux \left(9x + 6\right) - 12x^2 - 4x}{u \left(1 - u\right)^3 \left[u^3 + u^2 x (3x - 1) + 3ux^2 + x (3x + 1)\right]} \times du, \tag{25}
\]
by integration of which one obtains the WV size distribution function:

\[
g'(u) = u^\sigma (1 - u)^{-\alpha}(u + b)\beta((u^2 + cu + d)^\gamma \exp\left(\frac{\omega}{1 - u}\right) \times \exp\left[\frac{\epsilon - \gamma c}{\sqrt{d - c^2/4}} \tan^{-1}\left(\frac{u(c/2)}{\sqrt{d - (c^2/4)}}\right)\right],
\]

(26)

with the magnitudes of the power indices, \(\sigma, \alpha, \beta, \gamma,\) and coefficients \(\epsilon, \gamma,\) and \(d\) expressed through the parameter \(x\) are given in the appendix.

3. Results and Discussion

The WV distribution is represented in Figure 2. Dependences represented in Figure 2(a) are computed with interval \(\Delta x = 0, 1\). The same dependences normalized by their maxima are represented in Figure 2(b). In the normalized form, such dependences are well behaved for comparison with the normalized experimentally obtained histograms.

The results of comparison of the experimentally obtained histograms with our computations, (23), are shown in Figure 3 for various magnitudes of the parameter \(x\). All experimentally obtained histograms and theoretically found dependences are normalized by their maxima. For convenience, the LS distribution is represented, accurate within a constant, as a function of variable \(u = r / r_g\):

\[
g'(u) = u^2 (1 - u)^{-11/3}(u + 2)^{-2/3} \exp\left(-\frac{1}{1 - u}\right).
\]

(27)

Experimentally obtained histograms shown in Figure 3 correspond to the size distribution function of Al\(_3\)Sc NCs in binary alloys Al–Sc\((0,12\text{ am}\%\text{Sc})\). Exposition of alloys has been performed at temperature 350°C over a period: (a) 2; (b) 5; (c) 72; (d) 104; (e) 168 h [32]. Dashed curves correspond to the LS, \(W(x = 0)\), and \(V(x = 1)\) distributions. Solid curve corresponds to the WV distribution for relevant magnitudes of the parameter \(x\). One can see that neither the W distribution \((x = 0)\) nor the V distribution \((x = 1)\) is well fitting the experimentally obtained histograms. The LS distribution (dashed curve) and the WV distribution for relevant magnitude of the parameter \(x\) (solid curve) fit experimentally obtained histograms much more reliably. Moreover, one can see from Figure 3 that the WV distribution (23) provides better fitting of experimental data than the LS distribution.

The same is observed for alloys Al(Sc,Zr). Histograms in Figure 4 correspond to size distribution of NCs Al\(_3\)Sc\(_{1-x}\)Zr\(_x\) in such alloys [33]. Alloys (Al-0,14Sc-0,012Zr)am% were exposed at temperature 375°C over a period: (a) 3; (b) 192; (c) 288 h. Similarly to the case of binary alloys, the WV distribution (23) satisfactorily fits experimentally obtained histograms. It means that the proposed mechanism of cluster coarsening governed by two mechanisms \((w \text{ and } l\text{ sones})\) in parallel is realized under the OR. For that, interpretation of experimentally obtained histograms is made by applying the WV distribution.

4. Conclusions

Summarizing, it has been shown that the modified Lifshitz-Slyozov-Wagner (LSW) theory [4, 5] can be applied to nanocluster systems. Theory of the Ostwald's ripening for alloys containing nanocrystalline phases must be assumed taking into account not only diffusion flow, \(j_d\), but also kinetic (Wagner's) one, \(j_k\). It has been shown, for alloys containing Al–Sc and Al(Sc,Zr), correspondingly, NCs Al\(_3\)Sc and Al\(_3\)(Sc\(_{1-x}\)Zr\(_x\)), that the size distribution function is satisfactorily fitted by the introduced Wagner-Vengrenovich (WV) distribution here.
Figure 3: Comparison of experimentally obtained histograms of Al₃Sc NCs [32] with the WV distribution (solid curve) for exposition of alloys for temperature 350°C over a period: (a) 2; (b) 5; (c) 72; (d) 104; (e) 168 h.
Figure 4: Comparison of experimentally obtained histograms of Al$_3$Sc$_{1-x}$Zr$_x$ NCs [33] with the WV distribution (solid curve) for exposition of aluminium-based alloys containing 0.14 Sc and 0.012 Zr at % for temperature 375°C over a period: (a) 3; (b) 192; (c) 288 h.

Appendix

To integrate (25) for determining $g'(u)$, one must perform prime factor decomposition of the third-order polynomial into denominator in respect of $u$

$$u^3 + u^2x(3x-1) + u3x^2 + x(3x+1)$$

$$= (u+b)(u^2 + cu + d), \quad (A.1)$$

where the root of the cubic equation (A.1), found using the Cardano formula, has the form:

$$b = \frac{\mu}{3} - w - \nu, \quad (A.2)$$

$$\mu = 3x^2 - x, \quad w = \sqrt{\frac{q}{2} + \sqrt{z}},$$

$$\nu = \sqrt{\frac{q}{2} - \sqrt{z}}, \quad q = \frac{2\mu^3}{27} - \frac{\mu s}{3} + t,$$

$$s = 3x^2, \quad t = 3x^2 + x, \quad z = \left(\frac{p}{3}\right)^3 + \left(\frac{q}{2}\right)^3,$$

$$p = \frac{3s - \mu^2}{3}, \quad (A.3)$$

and the coefficients are

$$c = \frac{2}{3}\mu + w + \nu, \quad (A.4)$$

$$d = \left(\frac{w+\nu}{2}\right)^2 + \left(\frac{w+\nu}{3}\right)\mu + \left(\frac{\mu}{3}\right)^2 + \frac{3}{4}(w-\nu)^2. \quad (A.5)$$

Taking into account (A.1), one obtains by integrating (25), the WV distribution (26), where
\[ \sigma = \frac{4x(3x+1)}{bd}, \]
\[ \alpha = (18x^2(b+1)(c+d+1)+11(b+c)+14bd+5) \times \left( (b^2+2b+1) \times (c^2+d^2+2cd+2c+d+1) \right)^{-1}, \]
\[ \gamma = \frac{\alpha - \sigma - \beta - 4}{2}, \quad \omega = -\frac{3}{(b+1)(c+d+1)}, \]
\[ \epsilon = \sigma(2-b-c)+\alpha(b-1) - \omega + \beta(2-c)+2\gamma(2-b). \]

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