Abstract- The disk brake may be a device for slowing or stopping the rotation of a wheel. Generally repetitive braking system of the automobile cars results in heat generation during each braking event. The brake disc brake 3D model prepared by CATIA software. Finite Element modal analysis of automobile 4 wheeler disc brake is performed to determine mode shapes and natural frequencies and also static analysis is performed to obtain optimized model from topology optimization technique from ANSYS 19 software. Hence, experimental testing using FFT analyzer technique (impact hammer and accelerometer) is performed to determine mode shapes and natural frequency and comparison of results with numerical results.

Keyword - Disc Brake, Topology Optimization, FFT Analyzer.

I. INTRODUCTION

The racing fans involved will surely know the importance of good brakes not just for safety but also for staying competitive. The disk brake may be a device for slowing or stopping the rotation of a wheel. A brake disc usually made from forged iron or ceramic composites includes carbon, Kevlar and silica, is connected to the wheel and therefore the axle, to prevent the wheel. A friction brake generates frictional forces as two or more surfaces rub against one another, to scale back movement. Based on the planning configurations, vehicle friction brakes are often grouped into drum and disc brakes. The main component of the braking system is the disk brake. Its performance directly affects the driving safety of the vehicle. When the vehicle is braking, the excitation frequency is close to the natural frequency of the brake disk, which will cause resonance, generate severe vibration & noise & affect ride comfort. Therefore, it is necessary to analyse modal characteristics of disk brake.

TATA Sumo 800 Lacer car disc brake was taken for experimental study purpose. The brake disc (or rotor) is that the rotating a part of a wheel's disk brake assembly, against which the restraint are applied. The material is usually gray iron, a sort of forged iron. The weight and power of the vehicle determines the necessity for ventilated disc.
IV. CAD DESIGN

Design parameters of TATA Sumo 800 Lacer car

- Disc Diameter = 260 mm
- Disc Material = Grey Cast Iron
- Disc Thickness = 12 mm
- Internal Diameter = 140mm
- Internal Thickness = 50 mm
- Hole Diameter = 10 mm 5Holes
- Pad brake Material = Asbestos
- Pad Dimension = 125 mm x 12 mm

Used CATIA software. CATIA is mechanical design software. CATIA users access the highest productivity for specific advanced processes with focused solutions.

- Sketcher
- Part design
- Assembly design
- Wireframe and surface design
- Drafting
- Analysis of disc brake in CATIA
- Meshing Structural Static & Modal analysis by ANSYS software

V. DESIGN CALCULATION

Input Parameter for Disc Brake of TATA Sumo 800 Lacer

| Parameter Name                  | Parameter Value (Unit) |
|---------------------------------|------------------------|
| Mass of Vehicle                 | 2625 Kg                |
| Speed of Vehicle                | 100 km/h = 27.7 m/s    |
| Wheel Diameter                  | 600 mm                 |
| Wheel Base                      | 2425 mm                |

Table 1: Basic Parameter of Vehicle

| Parameter Name                  | Grey Cast Iron         |
|---------------------------------|------------------------|
| Density                         | 7000 Kg/m$^3$          |
| Yield Tensile Strength          | 142 MPa                |
| Young Modulus E                 | 100 GPa                |
| Poisson Ratio $\nu$             | 0.28                   |
| Specific Heat, $C_p$            | 586 J/Kg.K             |
| Thermal Conductivity , $K$      | 54 W/m.K               |

Table 2: Properties of Grey Cast Iron

| Parameter Name                  | Parameter Value         |
|---------------------------------|-------------------------|
| Outer Diameter of Disc          | 260 mm                  |
| Inner Diameter of Disc          | 140 mm                  |
| Hole Diameter                   | 10 mm                   |
| Thickness of Disc               | 12 mm                   |
| Weight of Disc                  | 6.2 Kg                  |

Table 3: Disc Brake Dimensions

Calculation:

a) Kinetic Energy of Vehicle

$$K.E = \frac{M \times V^2}{2} = \frac{(2625 \times 27.72)^2}{2}$$

Where,

- K. E = kinetic Energy (J)
- M = Mass of vehicle (Kg)
- V = Linear velocity of vehicle (m/s)

b) Stopping distance of vehicle

Braking distance of vehicle refers to the distance a vehicle will travel from the point when its brakes are fully applied to when it comes to a complete stop.

The maximum friction force $F = \mu \times M \times g$

$$F = 0.7 \times 2625 \times 9.81$$

$$\mu = \frac{0.7 \times 2625 \times 9.81}{2}$$

$$F = 18025.8 N$$

c) Deceleration of the vehicle:

$$a = \frac{F}{M}$$

$$a = \frac{18025.8}{2625} = 6.86 \text{ m/s}^2$$

d) Time taken to stop the vehicle:

$$t = \frac{V}{a}$$

$$t = \frac{27.7}{6.86} = 4.037 \approx 4 \text{ s}$$

e) Distance cover

Maximum speed of vehicle is 27.7 m/s

So, distance covered by vehicle in 4 second is = $27.7 \times 4$

Stopping distance (SD) = 110.8 m

Now, following is other equation to calculate total stopping distance by considering reaction time of driver is [4]

Total Stopping distance (SD)

$$SD = (V \times \text{reaction time}) + (V_2/2 \times \mu \times g)$$

$$= (27.7 \times 4) + (27.72 / 2 \times 0.7 \times 9.81)$$

$$SD = 138.96 \text{ m}$$

So, by considering the average stopping distance is 124 m.
f) Breaking force
Brake force, also known as Brake Power, is a measure of braking power of a vehicle. Here following process is given to calculate exact force required to stop vehicle within stopping distance or stopping time. [4]
Tangential braking force: \( (BF) \)
\[ (BF)t = K \cdot E/(SD) \] (S D – stopping distance)
\[ = 1007068.125/124 \]
\( (BF)t = 8121.51 N \)
Tangential force on each wheel \( Ft \)
\[ Ft = (BF)/4 \] (4 indicate force on each wheel)
\[ = 8121.51/4 \]
\[ = 2030.3 N \]
Braking torque on wheel \( Tw \)
\[ Tw = Ft \times R \]
\[ = 2030 \times 0.300 \]
\[ = 609 N. m \]
Where, \( R \) – Radius of the tyre (m)
Effective Rotor radius \( Re \)
\[ Re = (Rotor diameter/ 2) − (caliper piston diameter/ 2) \]
\[ Re = (260/ 2) − (44/ 2) \] (Rotor diameter – 260 mm)
\[ Re = 103 mm = 0.103 m \]
Here, caliper piston diameter is 44 mm.

g) Braking torque on disc \( Tb \)
\[ Tb = Tw \times R/r \]
\[ = 609 \times 250/125 \] (Tw – 250 mm)
\[ Tb = 1218 N. m \]
h) Clamping force \( C \)
\[ C = Tb/2 \times \mu \times Re \]
\[ = 1218/2 \times 0.5 \times 0.103 \]
\[ C = 11825 N \]
Pressure applied by clamp force on pad = clamping force / area of pad
\[ = 11825 \times 5145 \times 2 \times 5145 \times 2 \] (Area of pad = 5145 mm²)
\[ = 2.29 MPa \]

VI. ANALYSIS
TATA Sumo 800 Lacer car disc brake is taken for analysis.
After designing disc brake rotors in CATIA V5 the profiles is imported to ANSYS Workbench for further analysis such as Static structural analysis, and Modal analysis.

Material Selection for Disc Brake – Grey Cast Iron

| Material Property | Value |
|-------------------|-------|
| Density           | 7.00 kg/m³ |
| Coefficient of Thermal Expansion | 1.25°C⁻¹ |
| Young’s Modulus   | 1.5 × 10^6 Pa |
| Poisson’s Ratio   | 0.30 |
| Shear Modulus     | 2.4 × 10^6 Pa |

Fig. 5 Engineering Material Properties in ANSYS

- **Geometry of Existing Disc Brake**
  - Fig. 6 Geometry of Disc Brake Imported In ANSYS

- **Meshing**
  - Meshing done by ANSYS software to reduced degree of freedom from Infinite to finite with the help of discretization or meshing (Nodes & Elements)

- **Boundary Conditions**
  - Fig. 8: Boundary Conditions for Disc Brake-MA
Disc brake is fixed at one end to determine the mode shape and natural frequency.

- **Modal Analysis:**

Modal analysis may be a technique to review the dynamic characteristics of a structure under vibrational excitation. Natural frequencies, mode shapes and mode vectors of a structure may be determined using modal analysis.

**Different Mode Shapes:**
The modal frequencies of the first five steps and modal shapes of each order shown in below figures:-

In above figures different mode shapes are plotted with respective natural frequency so, it is observed the mode shape pattern also change with respective frequency so maximum frequency is observed around 1446 N.

- **Static Structural Analysis**

Consider Velocity of Vehicle (V) = 80 km/hr = 22.22 m/s
Where,
V – Velocity of Vehicle
Diameter of Disc brake (d) = 0.26 m
Radius of Disc Brake (r) = 0.13 m
V = r x ω  
............. (ω – Angular velocity)
22.22 = 0.13 x ω
ω = 170 rad/s [4]

In above analytical calculation (A) pressure acting on pad is calculated as 2.29 MPa but design is for maximum condition so standard equation to calculate pressure on pad is given below

From paper mentioned standard equation is

$$ \omega(t) = 69.44 - 22.32\left(1 - \frac{3.274}{20}\right) $$

So, pressure on rubber pad is 4 MPa on both sides are applied.

So, we have 4 MPa and 2.29 MPa as per design. It is beneficial to use 4 MPa as design should sustain extreme pressure due to fluctuation of motion on disc brake.

- **Boundary Condition:**

In boundary condition following are forces, pressure is mentioned.

Fixed support is applied along circular bolt holes and across edges as per existing situation.
Pressure of 4 MPa as per calculated analytically is applied on both surface of caliper pad as shown in red region.
Rotational velocity of 170 rad/s = 80 km/h is applied indicated in yellow region.

- **Total Deformation Results**

Fig.10 Details of Boundary Conditions-SA

In boundary condition following are forces, pressure is mentioned.

Fixed support is applied along circular bolt holes and across edges as per existing situation.
Pressure of 4 MPa as per calculated analytically is applied on both surface of caliper pad as shown in red region.
Rotational velocity of 170 rad/s = 80 km/h is applied indicated in yellow region.
It is observed that maximum deformation is 0.0108 mm.

- **Equivalent Stress Results**

![Equivalent Stress Results](image)

Maximum stress observed is 16 MPa

VII. TOPOLOGY OPTIMIZATION

Topology optimization could also be a mathematical approach that optimizes material layout within a given design area, for a given set of loads and boundary conditions such the resulting layout meets a prescribed set of performance targets.

Basic Theory

There are three types of structure optimization,

- Size optimization
- Shape optimization
- Topology optimization

Three optimization ways in which correspond to the three stages of the merchandise design methodology, significantly the detailed design, basic design and conceptual design. Size optimization keeps the structural form and topology structure invariant, to optimize the varied parameters of structure, like thickness, section size of beam, materials properties; shape optimization maintains the topology structure, to vary the boundary of structure and form, explore for the foremost applicable structure boundary scenario and shape; topology optimization is to hunt out the foremost effective path of materials distribution throughout never-ending domain that meet the displacement and stress conditions in structure, produce a specific performance optimum. Thus, compared to size and shape optimization, topology optimization with more freedom degree and bigger design area, its greatest feature is below unsure structural form, keep with the well-known condition and a given load to work out a budget structure, every for the abstract sort of recent product and improvement design for existing product, it is the foremost promising side of structural optimization. For continuous structure topology optimization, there are some mature ways like: uniform technique, evolutionary structural optimization technique, variable density technique etc.

- **Boundary Condition**

In boundary condition of topology optimization exclusion region are boundary condition applied in static structural analysis these are excluded.

- **Equivalent Stress**

![Equivalent Stress](image)
VIII. EXPERIMENTAL TESTING

The experimental validation operation is finished by using FFT Operation testing (Fast Fourier Transform) analyzer. The FFT spectrum analyzer samples the input, computes the magnitude of its sine and cosine components, and displays the spectrum of these measured frequency components. The advantage of this system is its speed. Because System operation FFT spectrum analyzers measure all frequency components at identical time, the technique offers the likelihood of being persistently faster than traditional analog spectrum analyzers. This analysis will be expressed as a series operation. The fast Fourier transform could be a method of operation mathematical method for transforming a function of your time into a function of frequency. Sometimes it's described as system transforming from the time domain to the frequency domain. it's very useful for all method analysis of time-dependent.

FFT analysis
FFT is one main property in any sequence getting used generally. To find this property of FFT for any given sequence, many transforms are being employed. the most important issues to be noticed find this property are the time and memory management. Comparison is finished between the 2 algorithms with relevance the memory and time managements and therefore the better one is pointed. Comparison is between the two algorithms written, considering the time and memory because the sole main constraints. Time taken by the 2 transforms find the basic frequency is taken. At the identical time the memory consumed while using the 2 algorithms is additionally checked. Supported these aspects it's decided which algorithm is to be used for better results.

IX. SUMMARY

- Modal analysis of hydraulic brake is performed to get different mode shapes and natural frequency of existing 4-wheeler hydraulic brake.
- Static structural analysis of hydraulic brake is performed to see deformation and equivalent stress. It's observed around maximum deformation is 0.0108 mm and equivalent stress is 16.76 MPa.
- It's concluded that the region indicated in the pit in topology optimization provides information regarding removal of material from that area it's about 55.53% to original mass.

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