Explaining Word Embeddings via Disentangled Representation

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Abstract

Disentangled representations have attracted increasing attention recently. However, how to transfer the desired properties of disentanglement to word representations is unclear. In this work, we propose to transform typical dense word vectors into disentangled embeddings featuring improved interpretability via encoding polysemous semantics separately. We also found the modular structure of our disentangled word embeddings helps generate more efficient and effective features for natural language processing tasks.

1 Introduction

Disentangled representations are known to represent interpretable factors in separated dimensions. This property can potentially help people understand or discover knowledge in the embeddings. In natural language processing (NLP), works of disentangled representations have shown notable impacts on sentence and document-level applications. For example, Larsson et al. (2017) and Melnyk et al. (2017) proposed to disentangle sentiment and semantic of sentences. By manipulating sentiment factors, the machine can rewrite a sentence with different sentiment. Brunner et al. (2018) also demonstrated sentence generation while more focusing on syntactic factors such as part-of-speech tags. For document-level applications, Jain et al. (2018) presented a learning algorithm which embeds biomedical abstracts disentangling populations, interventions and outcomes. Regarding word-level disentanglement, Athiwaratkun and Wilson (2017) proposed mixture of Gaussian models which can disentangle meanings of polysemous words into two or three clusters. It has a connection with unsupervised sense representations (Camacho-Collados and Pilehvar, 2018) which is an active research topic in the community.

In this work, we focus on word-level disentanglement and introduce an idea of transforming dense word embeddings such as GloVe (Pennington et al., 2014) or word2vec (Mikolov et al., 2013b) into disentangled word embeddings (DWE). The main feature of our DWE is that it can be segmented into multiple sub-embeddings or sub-areas as illustrated in Figure 1. In the figure, each sub-area encodes information relevant to one specific topical factor such as Animal or Location. As an example, we found words similar to “turkey” are “geese”, “flock” and “goose” in the Animal area, and the similar words turn into “Greece”, “Cyprus” and “Ankara” in the Location area.

Figure 1: Disentangled embedding with factors Animal, Location and Unseen.

We also found our DWE generally satisfies the Modularity and Compactness properties proposed by Higgins et al. (2018) and Ridgeway and Mozer (2018) which can be a definition of general-purpose disentangled representations. Also, our DWE can have the following advantages:

- **Explaining Underlying Knowledge**  
The multi-senses of words can be extracted and separately encoded despite the learning algorithm of the original word embeddings (e.g. GloVe) does not disambiguate. As a result, the encoded semantic can be presented in an intuitive way for examination.

- **Modular and Compact Features**  
Each sub-area of our DWE can itself be informative features. The advantage is that people
are free to abandon features in sub-areas irrelevant to the given downstream tasks while still achieving competitive performance. In Section 4, we show that using the compact features is not only efficient but also helps improve performance on downstream tasks.

- Quality Preservation

In addition to higher interpretability, our DWE preserves co-occurrence statistics information in the original word embeddings. We found it also helps preserve the performance on downstream tasks including word similarity, word analogy, POS-tagging, chunking, and named entity recognition.

2 Obtaining Disentangled Word Representations

2.1 Problem Definition

Our goal is transforming \( N \)-dimensional dense word vectors \( X \in \mathbb{R}^{N \times d} \) into disentangled embeddings \( Z \in \mathbb{R}^{N \times d} \) by leveraging a set of binary attributes \( A = \{ a_1, ..., a_M \} \) labelled on words.

\( Z \) is expected to have two properties. The first one is preserving word features encoded in \( X \). More specifically, we require \( X X^T \approx Z Z^T \) as pointed out by Levy and Goldberg (2014) that typical dense word embeddings can be regarded as factorizing co-occurrence statistics matrices.

The second property is that \( Z \) can be decomposed into \( M+1 \) sub-embedding sets: \( Z_{a_1}, ..., Z_{a_M} \) and \( Z_{unseen} \), where each sub-embedding set encodes information only relevant to the corresponding attribute. For example, \( Z_{a_1} \) is expected to be relevant to \( a_1 \) and irrelevant to \( a_2, ..., a_M \). Information in \( X \) not relevant to any attributes in \( A \) is then encoded in \( Z_{unseen}. \) An example of transforming \( X \) into \( Z \) with two attributes, Animal and Location, is illustrated in Figure 1.

For modelling the relevance between sub-embeddings and attributes, we use mutual information \( I(Z_a, a) \) as learning objectives, where \( a \) is an arbitrary attribute in \( A \).

2.2 Transformation with Quality Preservation

We obtain \( Z \) by transforming \( X \) by a matrix \( W \in \mathbb{R}^{d \times d}. \) That is, \( Z = X W. \) To ensure \( X X^T \approx Z Z^T, \) an additional constraint \( W W^T = I, \) is included. \( Z Z^T = (X W)(X W)^T = X(W W^T)X^T = X X^T \) if \( W W^T = I \) holds.

2.3 Optimizing \( I(Z_a, a) \)

Let \( z_{a,i} \) be the \( i \)-th row in \( Z_a. \) By derivation, \( I(Z_a, a) = \sum_{i=1}^{N} p(z_{a,i}) \log p(a|z_{a,i}) - \log p(a) \)

We let \( p(a) \) be constant and replace \( p(a|z) \) with a parametrized model \( q_\theta (a|z), \) By experiments, we found logistic regression with parameter \( \theta \) is sufficient to be \( q_\theta (a|z). \) Intuitively, high \( I(Z_a, a) \) means \( Z_a \) are informative features for a classifier to distinguish whether words has attribute \( a. \)

When increasing \( I(Z_a, a) \) by optimizing \( q_\theta (a|z) \), we found a strategy helping generate higher quality \( Z. \) The strategy is letting \( Z_a \) be features to reconstruct original vectors for words having attribute \( a. \) For words with \( a, \) the approach becomes a semi-supervised learning architecture which attempts to predict labels and reconstruct inputs simultaneously.

The loss function \( L(W, \theta, \phi) \) for maximizing \( I(Z_a, a) \) is as follow:

\[
-\frac{1}{N} \sum_{i=1}^{N} q_\theta (a|z_{a,i}) + \lambda \sum_{a,i} ||x_i - \phi (z_{a,i})||_2^2
\]

\( \mathbb{I}_{a,i} = \begin{cases} 
1 & \text{when } i \text{-th word has attribute } a \\
0 & \text{when } i \text{-th word does not have } a
\end{cases} \)

where \( \phi \) is single and fully-connected layer, \( x_i \) is the original \( i \)-th word’s vector in \( X, \) and \( \lambda \) is a hyper-parameter. We set \( \lambda = \frac{1}{2} \) in all experiments.

2.4 Learning to Generate Sub-embedding \( Z_a \)

As discussed in 2.3 that high \( I(Z_a, a) \) indicates \( Z_a \) are informative features for classification, we propose to regard sub-embedding generation as a feature selection problem. More specifically, we apply sparsity constraint on \( Z. \) Ideally, when predicting \( a, \) a smaller number of dimensions of \( Z \) are selected as the informative features, which are regarded as \( Z_a. \)

In this work, we use Variational Dropout (Kingma et al., 2015; Molchanov et al., 2017) as the sparsity constraint. At each iteration of training, a set of multiplicative noise \( \xi \) is sampled from a normal distribution \( \mathcal{N}(1, \alpha_\xi = \frac{\alpha_p}{1 - \alpha_p}) \) and injected on \( Z. \) That is, the prediction and reconstruction is done by \( \theta (\xi \odot Z) \) and \( \phi (\xi \odot Z). \) The parameter \( \alpha_\xi \in \mathbb{R}^d \) is jointly learned with \( W, \theta, \) and \( \phi. \) Afterwards, \( d \)-dimensional dropout rates
$p_a = \text{sigmoid}(\log \alpha_a)$ can be obtained. For each attribute $a$ in $A$, the dimensions with dropout rates lower than 50% are normally regarded as $Z_a$.

We would like to emphasize that the learned dropout rates are not binary values. Therefore, deciding the length of sub-embeddings can actually depend on users’ preferences or tasks requirements. For example, users can obtain more compact and pure $Z_a$ by selecting dimensions with dropout rates lower than 10%, or get more thorough yet less disentangled $Z_a$ by setting the threshold be 70%.

To encourage disentanglement when handling multiple attributes, we include additional loss functions on dropout rates. Let a $M$-dimensional vector $P$ be $1 - p_a$ for all $a$ in $A$ in a specific dimension. The idea is to minimize $\prod_{i=1}^{M} P_i$ with constraint $\sum_{i=1}^{M} P_i = 1$. The optimal solution is that the dimension is relevant to only one attribute $a'$ where $1 - p_a' \approx 1$. In implementation, we minimize the following loss function

$$\sum_{i=1}^{M} \log P_i + \beta ||\sum_{i=1}^{M} P_i - 1||^2_2 \tag{2}$$

We set $\beta = 1$ in the experiments, and equation 1 and 2 are optimized jointly.

To generate $Z_{\text{unseen}}$, we initially select a set of dimensions and constrain their dropout rates be always larger than 50%. The number of dimensions of $Z_{\text{unseen}}$ is a hyper-parameter. After selection, we do not apply equation 2 on the selected dimensions.

3 Evaluation

3.1 Word Embeddings and Attributes

We transform 300-dimensional GloVe\(^1\) into DWE. The 300-dimensional GloVe is denoted by GloVe-300. For word attributes $A$, we use labels in WordStat\(^2\). WordStat contains 45 kinds of attributes labeled on 70,651 words. Among the attributes, we select 5 high-level and easily understandable attributes: Artifact, Location, Animal, Adjective (ADJ) and Adverb (ADV) for our experiments. The number of words labelled with these 5 attributes is 13,337. After training, all pre-trained GloVe vectors are transformed by the learned matrix $W$ (i.e., $XW$) for downstream evaluations.

The number of learned dimensions for each attribute is illustrated in Figure 2, where the threshold of dropout rates for dimension selection is 50%.

3.2 Evaluation of Quality Preservation

We firstly examine whether DWE can preserve features encoded in GloVe-300. The examination is done by intrinsic evaluations including the following tasks and datasets.

- Word Similarity: Marco, Elia and Nam (MEN) (Bruni et al., 2014) and SimLex-999 (Hill et al., 2015).
- Word Analogy: Bigger Analogy Test Set (BATS) (Gladkova et al., 2016), Google Analogy (GA) (Mikolov et al., 2013a).
- POS tagging, Chunking and Named Entity Recognition (NER): CoNLL 2003 (Sang and Meulder, 2003; Li et al., 2017).
- QVEC-CCA\(^3\) (Tsvetkov et al., 2015): The performance is measured by semantic and syntactic CCA.

As shown in Table 1, 2 and 3, DWE can preserve performance of GloVe-300 on various NLP tasks. Probably due to the additional information of word attributes, DWE can have slightly better performance than GloVe-300 on seven of the tasks.

3.3 Attribute Classification

We design an attribute classification task for examining whether the DWE can meet requirements described in Section 2.3. We use logistic regression and take sub-embeddings $Z_a$ as input features for

\(^1\)https://nlp.stanford.edu/projects/glove/
\(^2\)https://provalisresearch.com/products/content-analysis-software/
\(^3\)https://github.com/ytsvetko/qvec
verifying the performance of classification by cross-validation. For each attribute, we randomly sample 400 data for testing. The numbers of positive and negative data for testing are balanced. Therefore, a random predictor would get around 50% accuracy in each classification task.

The binary classification accuracies are shown in Table 4. Take the second column of Table 4 for example. For distinguishing whether a word can be location, taking \( Z_{\text{location}} \) as features for training a classifier achieves the highest accuracy 83.8%. On the other hand, the accuracy reported in the second row of Table 4 implies that \( Z_{\text{location}} \) are less informative features for other attributes. Similar results can also be observed for other attributes.

### 3.4 Disentangled Interpretability

We provide some examples to demonstrate that words having ambiguous or different aspects of semantics can be disentangled. Table 5 shows the results of nearby words. As can be seen, querying a word in \( Z_\omega \) with different attributes can help discover the ambiguous semantics implicitly encoded in the original word vectors \( X \). The results also show that \( Z_{\text{unseen}} \) does capture meaningful information having little relevance to given attributes.

### 4 Application: Compact Features for Downstream Tasks

Here we demonstrate an application of the modularity and compactness properties of our DWE. We firstly aim to show the sub-embeddings can directly be informative features and can outperform GloVe with the same number of dimensions. With the high interpretability, selecting relevant sub-embeddings could be intuitive. Secondly, we will demonstrate that if deciding to fine-tune word vectors for a given downstream task, by using our DWE, we can focus on updating the relevant sub-embedding instead of the whole embedding. The advantage is that it reduces the number of learning parameters. Also, it could be regarded as a dimensional and interpretable regularization technique reducing overfitting.

We take a sentiment analysis task, IMDB movie review classification (Maas et al., 2011), for experiments. Intuitively, \( \text{ADJ} \) and \( \text{ADV} \) should be the most relevant attributes in \( \mathcal{A} \). We then select 50 dimensions from \( Z \in \mathbb{R}^{300} \) with the lowest dropout rates in \( \text{ADJ} \) and \( \text{ADV} \) sub-areas for comparing with 50-dimensional GloVe (GloVe-50). The embeddings with the selected dimensions are denoted by \( Z_{\text{adj}} + \text{adv} - 50 \). When tuning our DWE with the classifier, we update the 52 dimensions (\( Z_{\text{adj}} \in \mathbb{R}^{23} \) and \( Z_{\text{adv}} \in \mathbb{R}^{29} \)) of DWE and compare it with GloVe-300.

The document representations for classification is averaged word embeddings. The classifier is a logistic regression. When tuning the input word embeddings, we update the embeddings with gradient propagated from the classifier.

The results are listed in Table 6. From the table, we can see \( Z_{\text{adj}} + \text{adv} - 50 \) directly outperforms GloVe-50 without tuning. A possible explanation is that GloVe-50 is forced to encode information less relevant to the sentiments, making it less effective than \( Z_{\text{adj}} + \text{adv} - 50 \) in this task.

In the fine-tuning experiments, DWE can show slightly higher accuracy than GloVe-300 by updating only 52 instead of 300 dimensional features.

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1. https://nlp.stanford.edu/projects/glove/
| Feature          | Without Tuning | After Tuning |
|------------------|----------------|--------------|
| GloVe-50         | 76.55          | 86.72        |
| \(Z_{adj+adv}-50\) | 79.78          | 87.60        |
| GloVe-300        | 83.85          | 87.72        |
| DWE              | 83.67          | 87.84        |

Table 6: Classification accuracies (%) on IMDB dataset.

5 Conclusion

In this work, we propose a new definition and learning algorithm for obtaining disentangled word representations. As a result, the disentangled word vectors can show higher interpretability and preserve performance on various NLP tasks. We can also see the ambiguous semantics hidden in typical dense word embeddings can be extracted and separately encoded. Finally, we showed the disentangled word vectors can help generate compact and effective features for NLP applications. In the future, we would like to investigate whether similar effects can be found from non-distributional or contextualized word embeddings.

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