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Irodotou, Dimitrios and Thomas, Peter A (2021) Using angular momentum maps to detect kinematically distinct galactic components. Monthly Notices of the Royal Astronomical Society, 501 (2). pp. 2182-2197. ISSN 0035-8711

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Using angular momentum maps to detect kinematically distinct galactic components

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ABSTRACT

In this work, we introduce a physically motivated method of performing disc/spheroid decomposition of simulated galaxies, which we apply to the EAGLE sample. We make use of the HEALPIX package to create Mollweide projections of the angular momentum map of each galaxy’s stellar particles. A number of features arise on the angular momentum sphere which allows us to decompose galaxies and classify them into different morphological types. We assign stellar particles with angular separation of less/greater than 30° from the densest grid cell on the angular momentum sphere to the disc/spheroid components, respectively. We analyse the spatial distribution for a subsample of galaxies and show that the surface density profiles of the disc and spheroid closely follow an exponential and a Sérsic profile, respectively. In addition discs rotate faster, have smaller velocity dispersions, are younger and are more metal rich than spheroids. Thus, our morphological classification reproduces the observed properties of such systems. Finally, we demonstrate that our method is able to identify a significant population of galaxies with counter-rotating discs and provide a more realistic classification of such systems compared to previous methods.

Key words: galaxies: bulges – galaxies: evolution – galaxies: formation – galaxies: kinematics and dynamics – galaxies: structure.

1 INTRODUCTION

Exploring how and when galactic components form is an essential step towards understanding the formation and evolution of galaxies. Hence, a method that not only accurately identifies the constituent stellar populations but provides an additional way of exploring their dynamics is of great importance. The plethora of methods as presented below shows the usefulness of decomposing either observed or simulated galaxies, and the purpose of this work is to introduce a pioneering method of detecting kinematically distinct components and exploring their properties.

Photometric decompositions have been long used for splitting distinct stellar populations. A central component (‘bulge’) is separated from an extended one (‘disc’) with the use of different photometric profiles; however different methods can lead to variations in the contributions from each component (Cook et al. 2020). Various software packages (e.g. GIM2D, GALFIT, BUDDA, and IMFIT, see Simard et al. 2002; Peng et al. 2002; de Souza, Gadotti & dos Anjos 2004; Erwin 2015, respectively) allow the fit of a single- or double-component models and provide a plethora of profiles (e.g. Nuker law, Sérsic (de Vaucouleurs) profile, exponential, Gaussian, or Moffat/Lorentzian functions). This allows some of these codes to perform multicomponent decomposition and identify, in addition to a disc and a bulge; nuclear rings, lenses, and bars.

Many methods of bulge/disc decomposition in simulated galaxies have been proposed. One method assumes that the bulge has zero net angular momentum, hence estimates the disc-to-total ($D/T$) ratio by assigning to the bulge the sum of the mass of the counter-rotating particles multiplied by 2. This method has been extensively used (e.g. Crain et al. 2010; Clauwens et al. 2018; Trayford et al. 2019) even though it contains a crude assumption regarding bulge kinematics. A different method (Abadi et al. 2003) follows a kinematic decomposition in order to estimate the $D/T$ ratio of simulated galaxies by analysing the circularity of the orbits of stellar particles. This is defined (for a given stellar particle) as the ratio between the component of the angular momentum which is normal to the rotation plane and the maximum angular momentum for a stellar particle with the same binding energy (i.e. if on a circular orbit in the rotation plane). Many authors combined this idea with additional (spatial and/or binding energy) criteria in order to assign stellar particles to disc, bulge, and inner/outer halo components (Tissera, White & Scannapieco 2012; Cooper et al. 2015; Pillepich, Madau & Mayer 2015; Monachesi et al. 2019; Rosito et al. 2019). These attempts to more accurately identify distinct components unavoidably increase the complexity and free parameters of the decomposition. Finally, Gargiulo et al. (2019) introduced a hybrid technique that combines spatial and kinematic criteria in order to study bulges. However, as noted by Joshi et al. (2020), this method (i.e. the circularity parameter) does not always agree with visual classifications of morphology.

A new era of decomposition software utilizes machine-learning techniques to train neural networks to identify the correct profiles for each component (e.g. Dimarco et al. 2018). For example, a method introduced by Domínguez-Sánchez et al. (2018) classified Sloan Digital Sky Survey (SDSS) morphology based on Convolution Neural Networks, while Du et al. (2020) introduced a machine-learning algorithm to identify kinematic structures in IllustrisTNG galaxies.
Lastly, citizen-based projects like Galaxy Zoo (Masters & Galaxy Zoo Team 2020) follow a different path by allowing volunteers to perform the decomposition (Lingard et al. 2020).

The aim of this paper is to present a new decomposition method and compare galactic and component properties with local ($z \sim 0.1$) observational data. Our method not only provides a physically motivated spheroid/disc decomposition framework, but is also able to identify (in some cases multiple) kinematically distinct components based on their detailed representation on the angular momentum sphere. This gives one the unique ability of visually inspecting the angular momentum space of galaxies and utilizing this information to study the imprint of secular (Kormendy & Kennicutt 2004) and violent (Toomre 1977) processes on the constituent stellar components.

This paper is organized as follows. In Section 2, we describe our sample and introduce our method. In Section 3, we present a sample of angular momentum maps drawn from the EAGLE simulation and characterize the main morphological types. A detailed analysis of our spheroid-disc decomposition is presented in Section 4, a discussion regarding counter-rotating discs is presented in Section 5, and our conclusions are summarized in Section 6.

## 2 METHODOLOGY

In Section 2.1, we describe how we select galaxies for our study, and in Section 2.2, we describe the decomposition into spheroid and disc components on the basis of the angular momentum distribution of the stellar particles.

### 2.1 The galaxy sample

We apply our method to the RefL0100N1504 flavour of the EAGLE simulation (Schaye et al. 2015; Crain et al. 2015). We define galaxies as gravitationally bound substructures within Friends of Friends (FoF) structures (i.e. they consist of particles that share the same subgroup and group number, The EAGLE team 2017), where the former are identified by the SUBFIND algorithm (Springel et al. 2001).

We focus on galaxies with stellar masses $M_{\text{st}} > 5 \times 10^8 M_{\odot}$ where $M_{\text{st}}$ represents the stellar mass within a 30 kpc spherical aperture and we exclude all particles with separation more than 30 kpc from the galactic centre (defined as the position of the most bound particle). This guarantees that even the least massive galaxy is resolved with more than 3000 stellar particles. Although our method can be used for lower particle numbers, it will become less reliable as the particle number significantly drops below 3000, due to numerical effects which will lead to scattering of orbits.

### 2.2 Decomposition

The HEALPIX sphere (Gorski et al. 1999; Górski et al. 2002) is hierarchically tessellated into curvilinear quadrilaterals where the area of all grid cells at a given resolution is identical. We set $n_{\text{side}} = 2^4$ which is a parameter that represents the resolution of the grid (i.e. the number of divisions along the side of a base-resolution pixel). This results in 3072 HEALPix grid cells ($N_{\text{gc}} = 12n_{\text{side}}^2$) available over the sky which roughly corresponds to the same number of stellar particles our least massive galaxy has. In practice, our decomposition method follows the steps

1. We define the angular momentum vector of a stellar particle $i$ as

   $$\mathbf{J}_i = m_i (r_i - r_{\text{mb}}) \times (v_i - v_{\text{CoM}}),$$

   where $m_i$ is its mass, $r_i$ is its position vector, $r_{\text{mb}}$ is the position vector of the most bound particle (defined by SUBFIND), $v_i$ is the velocity vector of the particle, and $v_{\text{CoM}}$ is the velocity vector of the centre of mass defined as the collection of all stellar, gas, black hole, and dark matter particles that belong to same galaxy as particle $i$ and are within a 30 kpc spherical aperture centred on the potential minimum. We define the total stellar angular momentum vector as

   $$\mathbf{J} = \sum_{i=1}^{N} \mathbf{J}_i,$$

   where the summation goes over all stellar particles belonging to the corresponding galaxy.

2. We convert the angular momentum unit vector of all stellar particles from Cartesian to spherical coordinates (we use $\alpha \in [-180^\circ, 180^\circ]$ as the azimuth angle and $\delta \in [-90^\circ, 90^\circ]$ as the elevation angle) which we provide to HEALPIX in order to generate the pixelization of the angular momentum map.

3. We smooth the angular momentum map with a top-hat filter of angular radius $30^\circ$ and then identify the densest grid cell (i.e. the coordinates $(\alpha_{\text{den}}, \delta_{\text{den}})$ of the grid cell on the angular momentum sphere that contains most stellar particles).

4. We calculate the angular separation of each stellar particle from the centre of the densest grid cell as

   $$\Delta \theta_i = \arccos \left( \sin \delta_{\text{den}} \sin \delta + \cos \delta_{\text{den}} \cos \delta \cos (\alpha_{\text{den}} - \alpha) \right),$$

   where the index $i$ goes over all stellar particles belonging to the corresponding galaxy.

5. We assign to the disc component all stellar particles that satisfy

   $$\Delta \theta_i < 30^\circ,$$

   and the remaining particles to the spheroid. Hence, we directly select stellar particles based on their orbital plane. The choice of $30^\circ$ was motivated by the visual inspection of the angular momentum maps (see Section 3) and the work of Peebles (2020) who showed that for an axisymmetric disc with a flat rotation curve the eccentricity of a particle’s orbit can be written as

   $$\epsilon = 0.8 \cos(\theta),$$

   where $\theta$ is the angle that quantifies the tilt of the orbit with respect to the disc plane. For our $30^\circ$ criterion this results in particles with minimum value of $\epsilon \sim 0.7$, a limit commonly used for disc particles (e.g. Scannapieco et al. 2009; Marinacci, Pakmor & Springel 2014). In addition, our $30^\circ$ criterion results in good agreement and tight correlations with other commonly used morphological parameters (see Section 4.2 for more details).

6. Our method by construction will assign particles to the disc component even for the most idealized dispersion-supported system (i.e. a systems whose particle’s angular momenta will be perfectly uniformly distributed on the HEALPix sphere). That is because, even for an isotropic distribution over the sky, there will be a small fraction of particles whose angular momentum lies within $30^\circ$ of the nominal (directed) rotation axis. The following expression for the $D/T$ ratio

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1https://healpix.sourceforge.io

2We performed tests for $n_{\text{side}} = 2^i$ where $i = 4, 5, 6$ and there is no significant change in the $D/T$ ratios and the results presented in this work.
accounts for this ‘artificial’ increase of the disc component
\[
\frac{D/T_{\Delta \theta < 30^\circ}}{1 - \frac{\chi}{N_{all \ sky}} \left( \frac{N_{\Delta \theta < 30^\circ}}{N_{all \ sky}} - \chi \right)} = 1 - \cos(30^\circ), \tag{6}
\]

where \(N_{\Delta \theta < 30^\circ}\) and \(N_{all \ sky}\) are the number of stellar particles within \(30^\circ\) of the direction of the rotation axis and the whole sky, respectively, and
\[
\chi = \frac{1 - \cos(30^\circ)}{2}. \tag{7}
\]

Finally, we note that in this work we prefer not to limit the spatial extent of the spheroid (i.e. not split it into what is usually termed as a stellar halo and a bulge), since as recently discussed by Clauwens et al. (2018) and Gargiulo et al. (2019) there is no physical criterion that determines the boundary between a bulge and a halo. In addition we do not attempt to split the disc into a cold and warm (thin and think) component (Obreja et al. 2018). However, in a future work we intend to explore the imprint of such components on the angular momentum maps.

3 MORPHOLOGICAL CLASSIFICATION

In Section 3.1, we present angular momentum maps of the 100 most massive central EAGLE galaxies and classify them into distinct categories, and in Section 3.2, we study in more detail the maps of an example representative of each category, and compare three different methods of decomposing disc and bulge.

3.1 Distinct categories

Fig. 1 displays on a Mollweide, equal-area projection the angular momentum maps of the 100 most massive central (see The EAGLE team 2017) galaxies. For visual purposes, all particles have been rotated so that \(J_\star\) points towards the reader (see Appendix A). Several distinct categories of structure are visible:

(i) Rotationally supported systems: the simplest behaviour is a single cluster of dense grid cells (e.g. galaxy 39, 85, and 100), usually closely aligned with the total angular momentum of the galaxy, \(J_\star\). These are well-ordered disc-dominated galaxies. Interestingly, the majority of these (e.g. galaxy 25, 57, and 94) also show a slight antipolar excess of counter-rotating particles – we discuss this further in Section 5 below.

(ii) Dispersion-supported systems: these do not show a single, dominant density peak in the angular momentum map. There are a variety of morphologies:

(a) Double-peak systems: there are several examples of systems with two, distinct density peaks in the angular momentum maps, either relatively isolated (e.g. galaxy 18, 40, and 87), or buried within a great circle of orbits (e.g. galaxy 2, 46, and 70). For these galaxies, there is no well-defined, ordered rotation; hence they represent dispersion-dominated systems. Where two density peaks are visible, these tend to be opposite each other on the sky: in such an orientation the minor axes align and the mixing and precession of orbits in the merger remnant is heavily suppressed. They are likely the result of either a merger of progenitors with opposite angular momentum (Bender 1988; Krajnovi\'c et al. 2015) or the accretion of counter-rotating gas which settles and forms stars with angular momentum in the opposite direction (Vergani et al. 2007; Coccato et al. 2013; Algorry et al. 2014).

(b) Great circle systems: galaxies with a ring (great circle) of high-density points in the map (e.g. galaxy 34, 82, and 96); depending on the orientation of the galaxy it can appear as a horizontal S-shaped (e.g. galaxy 3, 19, and 65) or as a U (e.g. galaxy 5, 22, and 77) or upside down U (e.g. galaxy 20, 64, and 79). It is interesting to note that this great-circle structure is much more common than having orbits that are more uniformly distributed (e.g. galaxy 58, 72, and 90) across all directions in space. This is anticipated since mergers are not expected to mix orbits up evenly in phase space. Instead, realistic merger remnants have angular momentum distributions that are composed of varying contributions from different orbital families, such as short- and long-axis tube orbits (Valluri & Merritt 1998; Deibel, Valluri & Merritt 2011). Some of the dispersion-dominated systems (e.g. galaxy 5, 22, and 34) have a uniform density of orbits around a great circle, which reflects that for every direction in space there are roughly equal numbers of stellar particles with positive and negative angular momenta; others show a clear density peak (e.g. galaxy 20, 44, and 61) which suggests a relatively minor merger.

(iii) Multiple-peak (merging) systems: a very few systems show three or more density peaks (e.g. galaxy 14, 21, and 60). These are unlikely to be stable and may represent the early stages of mergers of a third galaxy on to a double-peaked system. It is beyond the scope of this work to study the formation path and evolution of such systems and their components, however we plan to do so in a future work.

3.2 Detailed kinematics

The first and fifth columns of Fig. 2 display on a Mollweide projection the angular momentum maps of galaxies representative of each one of the categories and subcategories identified in Section 3.1. In addition, for each galaxy it shows the grid cell density as a function of the angular separation from the densest grid cell (second and sixth columns) and from the angular momentum vector (third and seventh columns), and the distribution of the orbital circularity parameter (fourth and final columns). We follow Thob et al. (2019) and defined the latter for a given stellar particle \(i\) as
\[
\epsilon_i = \frac{L_{⊥,i}}{L_{⊥,\max}(E < E_i)}, \tag{8}
\]

where \(L_{⊥,i}\) is the component of the angular momentum which is perpendicular to the rotation plane and \(L_{⊥,\max}(E < E_i)\) the maximum value of the same component achieved by any stellar particle with binding energy less than that of particle \(i\). The red and blue hatched regions represent the distribution of the circularity parameter for bulge and disc particles defined as \(\epsilon < 0.7\) and \(\epsilon > 0.7\), respectively (Grand et al. 2017; Rosas-Guevara et al. 2020). The \(D/T_{\Delta \theta < 30^\circ}\) ratio for each galaxy in the second/sixth columns results from the method introduced in this work which assigns to the disc component stellar particles with \(\Delta \theta < 30^\circ\) and the remaining to the spheroid. The \(D/T_{Δθ=0}\) ratio shown for each galaxy in the third/seventh columns follows the assumption that the bulge has zero net angular momentum, hence its mass equals the mass of all counter-rotating particles multiplied by 2, and the remaining stellar particles are assigned to the disc component. Finally, the \(D/T_{Δθ>0.7}\) ratio produced for each galaxy following equation (8) is shown in the fourth/final columns.

(i) Galaxy 39: the majority of stellar particles have angular momenta well aligned both with the densest grid cell (second column) and the galactic angular momentum vector (third column). As
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Figure 1. A sample of the 100 most massive central galaxies in RefL0100N1504. In each panel, the red number on the top left corner refers to the galaxy's group number and the colour bar represents the number of particles per grid cell. Note that for visual purposes the galaxies have been rotated based on the process described in Appendix A.

discussed in Section 3.1, galaxy 39 is a rotationally supported galaxy since its ordered motion results in a relatively high $D/T\Delta \theta < 30^\circ$ ratio (0.49). This value is quite close to the $D/T_b=0$ and the $D/T_\epsilon > 0.7$ ratios (0.46 and 0.44, respectively).

(ii) Galaxy 25: an interesting example of a disc-dominated galaxy which has orbits in a plane, but they are not circular. This is reflected in its relatively high $D/T\Delta \theta < 30^\circ$ (0.52) and $D/T_b=0$ (0.56) ratios, but a considerably lower $D/T_\epsilon > 0.7$ ratio (0.03). Even though a well-ordered component appears as a second peak in the distribution of $\epsilon$, the strict criterion of $\epsilon > 0.7$ fails to include the disc component stellar particles with non-circular orbits. Hence, galaxy 25 (and of course others similar in nature) would have been misclassified by that method (see also discussion in Section 4.2).

(iii) Galaxy 18: the two density peaks on the angular momentum map are almost counter-rotating with respect to each other as can be seen on the $\Delta \theta$–density plane (second column). However, the picture is different when the angular separation is calculated from the angular momentum vector (third column) and not from the densest grid cell. Since neither of the structures are aligned with $\mathbf{J}$, particles from
both clusters of dense grid cells will contaminate the counter-rotating (grey shaded) region. This results in an artificial overestimation of the number of counter-rotating particles, hence a lower $D/T_{\Delta\theta=0}$ and $D/T_{\epsilon>0.7}$ ratios compared to $D/T_{\Delta\theta=30'}$. We discuss the effect of including counter-rotating particles in the definition of the disc component in Section 5.

(iv) Galaxy 14: there is a clear advantage of our method compared to the other ones presented in Fig. 2, which do not have the ability to identify three kinematically distinct components. The three distinct peaks on the $\Delta\theta$-density plane are not present in the last two panels corresponding to galaxy 14 on the fourth row.

(v) Galaxy 2: a perfect example of a balance between equal numbers of rotating and counter-rotating stellar particles. Galaxies with almost zero net rotation can be the result of either two counter-rotating structures or a uniform distribution of stellar orbits. Hence, in order to understand their formation one must first must accurately identify their distinct kinematic components. If the mechanism behind the formation of such galaxy is a merger of two counter-rotating galaxies (Hopkins et al. 2009; Lagos et al. 2018a) or accretion of counter-rotating gas, then the remnant disc should include both disc structures instead of none. Both $D/T_{\Delta\theta=0}$ and $D/T_{\epsilon<0.7}$ values are quite close to zero since these methods only use information regarding the total angular momentum of the galaxy. The inability of angular momentum based decomposition methods to reveal the true nature of such galaxies has been previously reported by Clauwens et al. (2018). However, our method is capable of identifying the two counter-rotating structures in opposite parts of the angular momentum sphere (embedded within a great circle), hence providing a more realistic D/T estimate – see also discussion in Section 5 where we investigate the inclusion of counter-rotating particles in our definition of D/T.

(vi) Galaxies 3, 5, and 20: these all represent dispersion-supported system as discussed in Section 3.1 and are similar in nature to galaxy 2, but with more asymmetry and a variety of strengths for the main density peak(s).

In summary, all galaxies apart from galaxy 39 and 25 have relatively similar $D/T$ ratios, however the imprint they leave on the angular momentum maps are far from similar. This means that their formation histories and the mechanisms that gave rise to these features were not identical. Identifying these kinematically distinct components gives one the ability to isolate and study them in more detail, in an attempt to understand galaxy formation and evolution, as we briefly do below.

### 3.3 Morphology of the individual components

Fig. 3 shows the face-on and edge-on projection of the disc and spheroid components identified by our method (see Section 2.2) for the sample of galaxies presented in Fig. 2. Galaxies 39 and 25 which are rotationally supported galaxies, have prominent spiral arms (face-on projections) and a well-defined thin discs (edge-on projections) akin to grand-design spiral galaxies. Galaxy 18, which showed as a
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Figure 3. The stellar surface density of the components identified by our method for the sample of the eight galaxies shown in Fig. 2. The red number on the top left corner in each row refers to each galaxy’s group number. The face-on and edge-on projections for the disc and spheroid are shown as indicated at top of each column.

double peak in Fig. 2, is seen to contain a very compact and elongated disc, similar to the dispersion-supported systems. The triple-peak nature of Galaxy 14 shows as a small subclump within the spheroid, but Galaxy 3 shows a much stronger asymmetry, suggestive of a more significant merger, but not evident in the kinematic analysis – that shows the importance of using more than one technique to characterize the structure of galaxies.

Investigating further the morphology of each component we explore their stellar mass distributions. Fig. 4 shows the stellar surface density radial profiles for the total stellar mass (black points) and for the disc (blue points) and spheroid (red points) components for the sample of the eight galaxies shown in Fig. 2 and sorted based on their $D/T/\Delta l_{\theta}<30$ values. These galaxies represent a blend of disc-dominated ($D/T/\Delta l_{\theta}>0.5$) and spheroid-dominated ($D/T/\Delta l_{\theta}<0.5$) galaxies. We perform a two-component fit of the face-on total stellar surface density by using a non-linear least-squares method to fit a double Sersic (1968) profile (black line) which consists of a 1D Sersic function and a fixed $n=1$ exponential profile:

$$
\Sigma(r) = \Sigma_{0,s} \exp \left[ -b_s \left( \frac{r}{R_{eff}} \right)^{1/n} \right] + \Sigma_{0,d} \exp \left[ -\left( \frac{r}{R_d} \right) \right],
$$

where $r$ is the projected 2D radius, $\Sigma_{0,s}$ and $\Sigma_{0,d}$ are the central surface densities of the spheroid and disc, respectively, $b_s$ is the Sersic coefficient parameter, $n$ is the Sersic index, $R_{eff}$ is the effective radius that encloses half of the projected total stellar mass, and $R_d$ is the disc scale length (see also Appendix B for more details). In addition, we fit independently the disc with an exponential profile (blue curve) and the spheroid with a Sersic profile (red curve).

Even though we do not restrict the physical extent of our components, we see a clear trend which holds for all galaxies in Fig. 4 and shows that the spheroid component dominates the mass budget in the central regions even for the disc-dominated galaxies; while we notice a drop in disc’s surface density in the central regions. This is in agreement with previous works (e.g. Obreja et al. 2013; Breda, Papaderos & Gomes 2020) who argued that disc components exhibit central intensity depression which lowers their contribution to the stellar mass. This drop indicates that it is easier for particles to scatter away from small $\Delta l_{\theta}$ near the centre (i.e. based on our method they do not have disk-like kinematics). In most cases, there is an increase in disc’s surface density between 3 and 7 kpc (right after the aforementioned drop) which partially exists due to contamination between the components.

In galaxy 25, we see that at $r \sim 20$ kpc, there is a prominent bump which appears both in the total (black points) and the disc (blue points) surface densities. This excess of stellar mass is related to spiral arms and reinforces our finding that galaxy 25 has spiral arms which our method correctly associates with its disc component (see Fig. 3). In general, the majority of spheroids tightly follow a Sersic profile especially in the central regions, while discs are well fitted by an exponential profile (even when they are subdominant components) particularly at their outskirts, as expected.

4 RESULTS

Having detailed the methodology and classification of our components, we present in this section relations between $D/T/\Delta l_{\theta,<30}$ and galactic/component properties for EAGLE galaxies selected as described in Section 2.1.

4.1 Correlations with galactic properties

In this work, we use the information depicted on angular momentum maps to estimate the relative mass contribution of each component to
In the first panel, we compare with the Zhu et al. (2018) that passive galaxies have lower spin parameters (at fixed stellar mass) as we move to higher or lower masses, galaxies tend to be more spheroid-dominated – in agreement with the observational data. A higher angular momentum.

Lastly, we find a weak trend between both the gas fraction and sSFR with $D/T_{\Delta \theta < 30^\circ}$, showing that more gas-rich and star-forming galaxies have preferentially more prominent disc components. These conclusions are in agreement with Lagos et al. (2018b) who found that (at fixed stellar mass) passive galaxies have lower spin parameters than star-forming ones.

4.2 Correlations with other methods

Even though it was originally assumed that early-type galaxies (ETGs) and (classical) bulges are solely pressure-supported systems, it was later revealed that they often do have some rotation (e.g. Bertola & Capacchioni 1975; Kormendy & Illingworth 1982; Davies et al. 1983; Scorza & Bender 1995; Emsellem et al. 2011). In general, galactic spheroids and ETGs are dominated by stars in low angular momentum orbits, while late-type galaxies (LTGs) are populated by stars performing ordered rotational orbits. Theoretical studies usually use the $D/T$ ratio to distinguish between ETGs and LTGs, hence the method used to perform the decomposition should be able to accurately capture the distinct kinematic components.

For that reason, we compare in Fig. 6 the $D/T_{\Delta \theta < 30^\circ}$ ratio with, from left to right, the $D/T_{J_b=0}$ ratio, the average circularity parameter ($\tau$), the ratio between rotation and dispersion velocities ($v_{rot}/\sigma$), and the fraction of stellar particles’ kinetic energy invested in corotation ($\kappa_{co}$ introduced by Correa et al. 2017). We find positive correlations between our method and the aforementioned ones, with the $D/T_{J_b=0}$ ratio showing the most scatter and $\kappa_{co}$ and $v_{rot}/\sigma$ the least. The latter curves over towards high $v_{rot}/\sigma$ values in disc-dominated systems, as has been recently reported by Thob et al. (2019).

We note that the $D/T_{\Delta \theta < 30^\circ}$ value where the demarcation (red) lines meet the median (black) lies lower than the 0.5 value used by some other methods (e.g. Rosito et al. 2018; Tissera et al. 2019; Rosito et al. 2019) to separate disc-dominated from bulge-dominated galaxies; and it is closer to that of, for example, Lagos, Cora & Padilla (2008), Weinzirl et al. (2009), Gargiulo et al. (2015), Pedrosa & Tissera (2015), Irodotou et al. (2019), Obreschkow et al. (2020), and Zanisi et al. (2020). Finally, we note that even though...
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4.3 Correlations with environment

Dense environments are prone to frequent mergers (Naab et al. 2014; Tacchella et al. 2019) which are the natural culprits for converting ordered motion to random orbits and lowering the angular momentum of the remnant (Hopkins et al. 2010; Lagos et al. 2018a; Jackson et al. 2020); this will also affect the $D/T_{\Delta\theta<30}$ ratios.

To study this effect, Fig. 7 shows, from left to right, the probability density function (PDF) for central and satellite galaxies (i.e. galaxies with subgroup number zero and greater than zero, respectively, based on the EAGLE nomenclature, McAlpine et al. 2016) and the dependence of the number of satellites, the misalignment between the angular momentum of the disc and the spheroid components, and of the stellar and the gaseous (defined following equations 1 and 2 but using gas particles instead of stellar) components on the $D/T_{\Delta\theta<30}$ ratio. Central and satellite galaxies share relatively similar distributions of $D/T_{\Delta\theta<30}$ ratios with preferred values between 0.2 and 0.5.

the four methods form tight relations with $D/T_{\Delta\theta<30}$, on some occasions we see a mismatch between the predictions which can lead in miss-classifications. These disagreements are responsible for the dispersion seen in Fig. 6 and are more prominent in the second panel, where a few ($\sim 20$) galaxies with $2<\epsilon<3$ appear well above the median and the 16th–84th percentile range. Such case is galaxy 25 (presented in Section 3.2) which has $\epsilon \sim 0.2$ and $D/T_{\Delta\theta<30} \sim 0.5$: hence the former method classifies it as an ETG and the latter as disc-dominated.

The fact that our method not only identifies such discrepancies but also provides a deeper insight and is able to explain them is what makes it unique. In addition, it differs from some previous methods since it does not contain any a priori assumptions regarding the kinematics of the components (e.g. that stellar particles counter-rotating with respect to the total angular momentum are bulge particles) hence, provides a more physically-motivated way of identifying kinematically distinct components.
However, there is a clear trend between the $D/T_{\Delta \theta_{<30}}$ ratios and the number of satellites which indicates that the more satellites a central galaxy has the more dominating its spheroid component is (i.e. lower $D/T_{\Delta \theta_{<30}}$ values); the well-known morphology–density relation. As far as the misalignment between the disc and spheroid components is concerned, the median line reveals a weak trend (which becomes more significant as the angular momentum vectors align) which indicates that aligned/counter-rotating components exist in more disc-/spheroid-dominated galaxies. Similar behaviour is present for the stellar and gaseous components, however with an additional weak trend as the two become more anti-aligned. The alignment (or not) between disc and spheroid, and stellar and gaseous components is linked to environmental effects (Scannapieco et al. 2009; Sales et al. 2012; Aumer, White & Naab 2014; Garrison-Kimmel et al. 2018; Park et al. 2019), and we intend to further investigate this behaviour in a future work.

4.4 Mass-specific angular momentum relation

The angular momentum of a galaxy determines its size, morphology, and contains information regarding its formation path (Cortese et al. 2016; Posti et al. 2018; Sweet et al. 2018). The relative contribution of the disc and spheroid components to the total mass has been shown to dictate where a galaxy lies on the mass-specific angular momentum plane (Romanowsky & Fall 2012; Fall & Romanowsky 2018; Tabor et al. 2019).

Fig. 8 shows the stellar specific angular momentum as a function of the stellar mass colour-coded by the $D/T_{\Delta \theta_{<30}}$ ratio. The grey squares and crosses represent galaxies from Obreschkow & Glazebrook (2014) and Mancera Piña et al. (2020), respectively, and the stars represent galaxies from Fall & Romanowsky (2018) colour-coded by their $D/T$ ratio.

(i) Obreschkow & Glazebrook (2014): a sample of 16 nearby spiral galaxies from the The H I Nearby Galaxy Survey (THINGS, Walter et al. 2008) selected based on their Hubble types T (from Sab to Scd) which were taken from the HyperLeda data base (Paturel et al. 2003).

(ii) Fall & Romanowsky (2018): a sample of 57 spirals, 14 lenticulars and 23 ellipticals decomposed following a 2D decomposition of

(iii) Mancera Piña et al. (2020): a large sample of nearby disc galaxies which contains 90 galaxies from the Spitzer Photometry & Accurate Rotation Curves (SPARC) (Lelli, McGaugh & Schombert 2016), 30 from the Ponomareva, Verheijen & Bosma (2016) sample, 16 from the Local Irregulars That Trace Luminosity Extremes, THINGS (Hunter et al. 2012), 14 from the Local Volume Hi Survey (Koribalski et al. 2018), 4 from the Very Large Array survey of Advanced Camera for Surveys Nearby Galaxy Survey Treasury galaxies (Ott et al. 2012) and 3 from the Westerbork H I Survey of

---

*Figure 7.* First panel: the $D/T_{\Delta \theta_{<30}}$ ratio PDF for central (brown) and satellite (cyan) galaxies and the $D/T_{\Delta \theta_{<30}}$ ratio as a function of the number of satellites (i.e. number of galaxies that share the same group number), third panel: misalignment between the angular momentum of the disc and the spheroid components, and fourth panel: misalignment between the angular momentum of the stellar and the gaseous components. In the last two panels, we attached two panels on top showing the PDF of the x-axis data. In addition, the orange lines and shaded regions represent the median and 16th–84th percentile range, respectively.

*Figure 8.* The stellar specific angular momentum as a function of the stellar mass colour-coded by the $D/T_{\Delta \theta_{<30}}$ ratio. The grey squares and crosses represent galaxies from Obreschkow & Glazebrook (2014) and Mancera Piña et al. (2020), respectively, and the stars represent galaxies from Fall & Romanowsky (2018) colour-coded by their $D/T$ ratio.
Irregular and Spiral Galaxies (van der Hulst, van Albada & Sancisi 2001).

We match extremely well both the tight mass-angular momentum relation and the $D/T$ ratio-dependent vertical colour gradient which implies that for a fixed stellar mass disc-dominated galaxies have higher angular momenta than spheroid-dominated ones.

Fig. 9 shows the specific angular momentum separately for the disc (red) and spheroid (blue) components as a function of their stellar mass. We compare our results with the following observational data sets:

(i) Fall & Romanowsky (2013): a sample of nearby bright galaxies of all types introduced in Romanowsky & Fall (2012).
(ii) Tabor et al. (2019): a sample of ETGs from the Mapping Nearby Galaxies at Apache Point Observatory (Bundy et al. 2015; Drory et al. 2015) selected from the Galaxy Zoo 2 catalogue (Willett et al. 2013) as objects with ‘smooth’ vote fraction $>0.7$.

We find an adequate agreement both with Fall & Romanowsky (2013) and Tabor et al. (2019) data sets. Similar to the disc-dominated galaxies in Fig. 8, the disc components follow a tight relation which is more constrained than the one spheroids follow. The wide scatter in the spheroid specific angular momentum can be also seen in the observational data where the two surveys cover different locations on the plot. This behaviour potentially reflects selection effects which bias the Tabor et al. (2019) sample in favour of low angular momentum objects since they studied ETGs, whereas Fall & Romanowsky (2013) analysed galaxies of different morphological types (Romanowsky & Fall 2012). Furthermore, disagreements between the two surveys are also expected since they deduced $D/T$ ratios following different techniques.

4.5 The baryonic Tully–Fisher and Faber–Jackson relations

The Tully & Fisher (1977) and Faber & Jackson (1976) relations reflect fundamental correlations between the stellar mass and kinematics of rotationally supported LTGs and pressure-supported ETGS, respectively. Given the similarities between the disc and spheroid components with LTGs and ETGs, respectively, we explore if our kinematically distinct components follow the aforementioned relations.

Fig. 10 shows the baryonic (McGaugh et al. 2000) Tully–Fisher (left-hand column) and Faber–Jackson (right-hand column) relations. The orange line represents bulge-dominated galaxies as objects with ‘smooth’ vote fraction $>0.7$. The grey squares and cyan line represent disc-dominated galaxies from Avila-Reese et al. (2008) and Oh et al. (2020), respectively. Bottom right panel: the galactic stellar mass as a function of the disc (blue) and spheroid (red) line-of-sight velocity dispersion (calculated within the half-mass radius). The cyan and orange lines represent the disc and bulge components, respectively, from Oh et al. (2020).
component affects its host galaxy kinematics becomes clear in the bottom left panel which shows the Tully–Fisher relation for the disc (blue) and spheroid (red) component of each galaxy. The disc components follow a well constrained behaviour, while spheroid components’ mass and rotational velocity are almost uncorrelated with a significantly larger scatter than the disc, as also found by Oh et al. (2020).

Furthermore, the galactic Faber–Jackson relation reveals a tight correlation between the stellar mass and velocity dispersion where galaxies with higher \( D/T/Delta_1theta < \) have lower \( sigma_0, e \) due to their higher degree of ordered rotation. In the bottom right panel we find, in agreement with Du et al. (2020), that discy (spheroidal) structures are formed from dynamically cold (hot) stellar particles. However, we notice that, while our results have similar slope to Oh et al. (2020), they show a slight offset in normalization. A possible explanation can be that Oh et al. (2020) calculated the velocity dispersion as the average flux-weighted velocity dispersion \( (sigma_0) \) of all spaxels inside the effective radius, where \( sigma_0 \) of each spaxel was extracted after fitting a Gaussian line-of-sight velocity distribution; whereas we, following Thob et al. (2019), estimate \( sigma_0, e \) as the remaining motion (after subtraction the ordered corotation component) in the disc plane.

4.6 Anisotropy parameter

The anisotropy of stellar orbits within a system (Binney & Tremaine 2008) can be quantified by the parameter:

\[
\beta = 1 - \frac{u_{\theta}^2 + u_{\phi}^2}{2u_r^2},
\]

(10)

where \( u_{\theta}, u_{\phi}, \) and \( u_r \) are the average azimuthal, polar, and radial components of the velocity of each stellar particle. Hence, different types of orbits result in different values of \( \beta \):

\[
\begin{align*}
\beta = -\infty, & \text{ orbits are circular.} \\
< 0, & \text{ orbits are tangentially biased.} \\
0, & \text{ orbits are isotropic.} \\
> 0, & \text{ orbits are radially biased.} \\
1, & \text{ orbits are radial.}
\end{align*}
\]

In order to study the orbital composition of our spheroids we use a more convenient form of the anisotropy parameter: \( \tau = e^{\beta - 1} \). Hence, the five cases described above now change to \( \tau = 0, 0 < \tau < 0.367, \tau = 0.367, 0.367 < \tau < 1, \) and \( \tau = 1 \), respectively.

Fig. 11 shows \( \tau \) as a function of the \( D/T/Delta_1theta < \) ratio. Stellar particles which form spheroids have slightly tangentially biased orbits for low \( D/T/Delta_1theta < \) values and gradually move to more isotropic orbits (i.e. \( \tau \) values closer to the black dashed line) as \( D/T/Delta_1theta < \) increases. In other words spheroid-dominated galaxies consist of stellar particles in tangentially biased orbits while spheroids within disc-dominated galaxies consist of spherical particles in isotropic orbits. This trend while present is quite weak hence agrees with the kinematic similarities between spheroid components and ETGs found by previous studies (see Kormendy 2016, for a review).

4.7 Black-hole spheroid mass relation

Tight relations between black hole and spheroid properties have been revealed in numerous studies and have been linked with the fact that they form in closely associated processes (Kormendy & Gebhardt 2001; Marconi & Hunt 2003; Greene, Ho & Barth 2008; Gadotti & Kauffmann 2009; Sani et al. 2011; Shankar et al. 2012).

Fig. 12 shows the relation between the spheroid and black hole masses. We compare with the Haring & Rix (2004) data. Fig. 12 shows the relation between the spheroid and black hole masses.3 We compare with the Haring & Rix (2004, sample of 30 nearby galaxies) data set. We find that our spheroids form an almost linear relation (in log-space) between the black hole and spheroid mass which extends to all masses; a behaviour which is in agreement with previous work (Beifiori et al. 2012; Graham 2012; McConnell & Ma 2013; Barber et al. 2016; Habouzit et al. 2020). Hence, we broadly match the Haring & Rix (2004) relation despite the different definitions and extraction techniques used to estimate the mass of the bulge/spheroid component.

It is worth noting that the free parameters of the EAGLE black hole model have been calibrated to match the black hole–bulge mass relation; however that was performed using both different data sets (i.e. McConnell & Ma 2013 instead of Haring & Rix 2004) and

3As discussed in McAlpine et al. (2016). The EAGLE team (2017) this is the summed mass of all black holes associated with each subhalo.
Identifying kinematically distinct galactic components

Figure 13. The average stellar formation expansion factor (top) and metallicity (bottom) of the disc (blue) and spheroid (red) component as a function of the component stellar mass. The black line and shaded region represent the median and 16th–84th percentile range, respectively.

different masses (i.e. Schaye et al. 2015; Crain et al. 2015 used the total stellar mass instead of the spheroid mass).

4.8 Age and metallicity relations

The age and metallicity of galactic components reflect their formation processes and time-scales (Gadotti 2009; Obreja et al. 2013; Trussler et al. 2020), hence distinct components should follow different relations.

Fig. 13 shows the mass–age and mass–metallicity relations for the disc and spheroid components. We use $\alpha_{\text{comp}}$ as a proxy for the age of each component, which we define as the average birth (i.e. at the time a stellar particle is born) scale factor for all stellar particles belonging to that component (The EAGLE team 2017). In addition, the metallicity of each component is defined as the sum of the mass-weighted metallicity $Z$ of all stellar particles belonging to that component, where $Z$ is the mass fraction of elements heavier than helium. At a given component stellar mass, there is a clear trend (based on the median lines) which shows that disc components are younger and more metal-rich than the spheroid components. In agreement with previous simulations (e.g. Naab et al. 2014; Park et al. 2019; Rosito et al. 2019; Wang et al. 2019) and observations (e.g. Bothun & Gregg 1990; Mancini et al. 2019).

Figure 14. The $D/T_{\Delta \theta < 30^\circ}$ ratio as a function of the $D/T_{\Delta \theta < 30^\circ}$ ratio. The black line and shaded region represent the median and 16th–84th percentile range, respectively and the green line represents the 1:2 ratio.

5 DISCUSSION

In this work, we follow the method introduced in Section 2.2 which decomposes galaxies by identifying kinematically distinct components. This method in order to be in agreement with previous observational and/or theoretical methods assigns to the disc component particles that have angular momenta broadly aligned with the galactic one (the angle between the two should not exceed 30°, see equation 4). However, as discussed in Section 3.2 and shown in Fig. 7, there are numerous galaxies whose anti-aligned particles also form a component which counter-rotates (with respect to the galactic angular momentum). It is clear that if these particles are also assigned to the disc component that will have a significant impact on the predicted $D/T$ ratio. In this section, we briefly investigate what effect such a method will have on our $D/T_{\Delta \theta < 30^\circ}$ ratios.

We follow exactly the same process as the one described in Section 2.2 however in step (v) we assign to the disc component particles with

$$\Delta \theta_i < 30^\circ$$

and

$$\Delta \theta_i > 150^\circ$$

This results in a new $D/T$ ratio which we call $D/T_{\text{CR}}$. In addition, we amend step (vi) and we apply to $D/T_{\text{CR}}$ a correction with two times $\chi$, to account for the second 30° patch on the angular momentum sphere.

Fig. 14 shows $D/T_{\text{CR}}$ as a function of $D/T_{\Delta \theta < 30^\circ}$. The majority of galaxies, especially the ones with $D/T_{\Delta \theta < 30^\circ}$ values higher than 0.2, follow tightly the 1:1 relation as indicated by the median line and 1σ region. Hence, in cases where there is no significant counter-rotating component the $D/T_{\Delta \theta < 30^\circ}$ values are not significantly altered.4 However, some galaxies, especially the low $D/T_{\Delta \theta < 30^\circ}$ ones, have a dramatic change in their $D/T$ ratios that is reflected on their $D/T_{\text{CR}}$

4Small fluctuations of order $10^{-2}$ between the two ratios are also expected due to the smoothing process which finds and uses grid cell centres within 30°. So there are particles within 30° which are not included in the smoothing but are used when estimating the mass of the component.
Figure 15. A sample of five galaxies selected so that each one has a ratio of $D/T_{CR}$ to $D/T_{\Delta \theta < 30^\circ}$ higher than 2. Each galaxy is represented by five panels as described below. The first column displays for each galaxy on a Mollweide projection the angular momentum maps, where the red number on the top left corner in each row refers to each galaxy’s group number. As in Fig. 1, the galaxies have been rotated so that $J_*$ (hollow X symbol) points towards the reader. The second and third columns have the face-on and edge-on projections, respectively, for the disc component when it is defined based the method described in Section 2.2. The fourth and fifth columns have the same projections, respectively, but when the disc component also includes counter-rotating particles (see the text for more details). The text in the each panel on the second and fourth columns represents the $D/T_{\Delta \theta < 30^\circ}$ and $D/T_{CR}$ ratios, respectively, for each galaxy.

values which can be as high as $\sim 2.8$ times their original $D/T_{\Delta \theta < 30^\circ}$ ratios.

Fig. 15 shows the angular momentum maps and the face-on and edge-on projections for the two different definitions of the disc component for a sample of five galaxies who display noticeable differences between their $D/T_{\Delta \theta < 30^\circ}$ and $D/T_{CR}$ ratios. It becomes apparent from the angular momentum maps of all five galaxies that two structures exist; one well aligned with the galactic angular momentum and the other counter-rotating with respect to the latter. From the second and third columns, we see that these galaxies
have thin rotationally supported discs which they continue to exist (although increase their height and diameter) when particles with $\Delta \theta > 150^\circ$ are included. The most interesting case is galaxy 1182 (fifth row) which has $D/T_{\Delta \theta < 30}$ value of 0.27, while its $D/T_{\Delta \theta}$ ratio is 0.57. Hence, in with the former definition is classified as a spheroid-dominated galaxy while with the latter a disc-dominated.

6 CONCLUSIONS

Being able to extract galactic components is vital in studying the galaxy as a whole. In this work, we use the information depicted on angular momentum maps (Section 2) to identify kinematically distinct components and study the imprint each component leaves on the properties of their host galaxy. We consider this method a useful addition to the literature since it results in components which are in agreement with the observed. Our main conclusions are as follows:

(i) We find a clear separation in angular momentum space of distinct components and classify galaxies into several morphological types (Section 3).
(ii) We demonstrate that even though we make no assumptions regarding the spatial extend of our components, they follow the expected spatial distribution and surface density profiles (Section 3.2).
(iii) We compare with other methods and find, in general, tight relations but also some interesting cases in which our method provides better classification: for example disc-like galaxies with particles on non-circular orbits. (Section 4.2).
(iv) Our method identifies a significant population of galaxies with counter-rotating discs embedded within them (Section 4.3).
(v) Our components have distinct angular momenta (Section 4.4), kinematics (Sections 4.5 and 4.6), and ages and chemical compositions (Section 4.8). Thus, our morphological classification reproduces the observed properties of such systems.

In a future work, we will use our method to study merging systems and galaxies with counter-rotating discs in order to better understand their formation path and evolution. In addition, we intend to explore possible imprint of other kinematically distinct components, such as bars and pseudo-bulges, on the angular momentum maps.

ACKNOWLEDGEMENTS

The authors contributed in the following way to this paper. DI undertook the vast majority of the coding and data analysis, and produced the figures. PAT supervised DI and together they drafted the paper. DI would like to acknowledge his family members for producing the figures. PAT supervised DI and together they drafted the paper. DI would like to acknowledge his family members for producing the figures. PAT supervised DI and together they drafted the paper.

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DATA AVAILABILITY

A PYTHON version of the method introduced in this article can be found at https://github.com/DimitriosIrodotou/Irodotou-Thomas-2021. The EAGLE data are publicly available and accessible at http://icc.dur.ac.uk/Eagle/database.php. The data underlying this article will be shared on reasonable request to the corresponding author.

The authors contributed in the following way to this paper. DI undertook the vast majority of the coding and data analysis, and produced the figures. PAT supervised DI and together they drafted the paper. DI would like to acknowledge his family members for producing the figures. PAT supervised DI and together they drafted the paper. DI would like to acknowledge his family members for producing the figures. PAT supervised DI and together they drafted the paper.
APPENDIX A: ROTATION MATRIX

We rotate the coordinate and velocity vectors of each galaxy’s stellar particle by applying to each vector the dot product of following rotation matrices:

\[
R_z = \begin{pmatrix}
\cos(\alpha) & \sin(\alpha) & 0 \\
-\sin(\alpha) & \cos(\alpha) & 0 \\
0 & 0 & 1 \\
\end{pmatrix},
\]

and

\[
R_y = \begin{pmatrix}
\cos(\delta) & 0 & \sin(\delta) \\
0 & 1 & 0 \\
-\sin(\delta) & 0 & \cos(\delta) \\
\end{pmatrix},
\]

where \(\alpha\) and \(\delta\) are the right ascension and elevation from the reference plane of the galactic angular momentum.

APPENDIX B: PROFILES

The exact value for the term \(b_n\) can be obtained by solving:

\[
\Gamma(2n) = 2\gamma(2n, b),
\]

where \(\Gamma\) and \(\gamma\) are the complete and incomplete gamma functions, respectively (Ciotti 1991). Useful approximations have been proposed by Prugniel & Simien (1997) and Ciotti & Bertin (1999), however in this work we follow MacArthur, Courteau & Holtzman (2003) and use the asymptotic expansion of Ciotti & Bertin (1999) for all \(n > 0.36\):

\[
b_n = 2n - \frac{1}{3} + \frac{4}{405n} + \frac{46}{25515n^2} + \frac{131}{1148175n^3} - \frac{2194697}{30690717750n^4} + O(n^{-5}).
\]

and the polynomial expression derived by MacArthur et al. (2003) for \(n \leq 0.36\):

\[
b_n = \sum_{i=0}^{m} \alpha_i n^i,
\]

where \(m\) is the order of the polynomial and \(\alpha_i\) are the coefficients of the fit which can be written as:

\[
\alpha_0 = 0.01945, \quad \alpha_1 = -0.8902,
\]
\[
\alpha_2 = 10.95, \quad \alpha_3 = -19.67, \quad \alpha_4 = 13.43.
\]

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