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Eruption and emplacement timescales of ignimbrite super-eruptions from thermo-kinetics of glass shards

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Super-eruptions generating hundreds of cubic kilometers of pyroclastic density currents are commonly recorded by thick, welded and lava-like ignimbrites. Despite the huge environmental impact inferred for this type of eruption, little is yet known about the timescales of deposition and post-depositional flow. Without these timescales, the critical question of the duration of any environmental impact, and the ensuing gravity of its effects for the Earth system, eludes us. The eruption and welding of ignimbrites requires three transects of the glass transition. Magma needs to: (1) fragment during ascent, (2) liquify and relax during deposition, agglutination and welding (sintering), and (3) quench by cooling into the glassy state. Here we show that welding is a rapid, syn-depositional process and that the welded ignimbrite sheet may flow for up to a few hours before passing through the glass transition a final time. Geospeedometry reveals that the basal vitrophyre of the Grey’s Landing ignimbrite underwent the glass transition at a rate of ~0.1°C·min⁻¹ at 870°C; that is, 30–180°C below pre-eruptive geothermometric estimates. Application of a 1-D cooling model constrains the timescale of deposition, agglutination, and welding of the basal vitrophyre to less than 1 h, and possibly even tens of minutes. Thermo-mechanical iteration of the sintering process indicates an optimal temperature solution for the emplacement of the vitrophyres at 966°C. The vitrophyres reveal a Newtonian rheology up to 46 MPa, which suggests that the ash particles annealed entirely during welding and that viscous energy dissipation is unlikely from loading conditions alone, unless shear stresses imposed by the overlying ash flow were excessively high and sustained over long distances. The findings underline the value of the term “lava-like” flow to describe the end rheology of Snake River-type ignimbrites, fully consistent with the typical lithofacies observed.

Keywords: ignimbrite volcanism, snake river plain, geospeedometry, glass transition, liquid relaxation, eruption timescale

INTRODUCTION

Large explosive (super-) eruptions of silicic magma commonly generate extensive pyroclastic density currents, preserved in the geologic record as ignimbrites, classically termed pumice-and-ash-flow tuff (Sparks, 1976; Sparks et al., 1978; Walker et al., 1981; Wilson and Walker, 1982; Walker, 1983; Wilson, 1985; Fisher et al., 1993; Freundt and Schmincke, 1995; Kobberger and Schmincke, 1999). During deposition from the pyroclastic density currents, agglutination, sintering, and welding of liquid globules of ash and pumice lapilli likely change the flow behavior from particulate to coherent and non-particulate (Brannen and Kokelaar, 1992; Gottsmann and Dingwell, 2001a). Architectural descriptions of high-grade ignimbrites often provide evidence for both syn- and post-depositional development of rheomorphic, ductile shear zones and “lava-like” lithofacies (Schmincke and Swanson, 1967; Chapin and Lowell, 1979; Brannen and Kokelaar, 1992; Moore and Kokelaar, 1998; Kokelaar and Koniger, 2000; Sumner and Brannen, 2002; Andrews and Brannen, 2011; Brown and Bell, 2013). Welding textures have been reported from a range of physical environments: in conduits (Tuffen et al., 2003; Tuffen and Dingwell, 2005; Noguchi et al., 2008; Kolzenburg et al., 2012; Lavallée et al., 2012), at the base of lava flows (Manley, 1992, 1995, 1996), in impact crater ejecta blankets (Dence, 1971; Kraut and French, 1971) and in ignimbrites, both proximal (Mellors and Sparks, 1991) and distal (Quane and Russell, 2005a; Andrews et al., 2008; Brannen et al., 2008; Brown et al., 2008; Trofimovs et al., 2008; Ellis et al., 2011). For the case of ignimbrites, two end-member stages of rheomorphism are postulated: syn-depositional/syn-welding flow (e.g., Brannen and Kokelaar, 1992; Andrews and Brannen, 2011) and late-stage
post-depositional compaction; welding and viscous flow (e.g., Schmincke and Swanson, 1967; Kobberger and Schmincke, 1999). Microstructural studies of the deformation history outlining the complex depositional dynamics of such rheomorphism have led to the former scenario being favored (Andrews et al., 2008; Andrews and Branney, 2011). The physico-chemical character of the deposits, especially where developing into shear zones, has direct rheological consequences for flow, where viscous energy dissipation may cause heating by tens if not hundreds of degrees (Robert et al., 2013). Recent work on ignimbrites has provided greatly improved, detailed, process-oriented descriptions of deposit formation (Andrews and Branney, 2011), but the timescales of deposition and post-depositional flow remain largely unconstrained. Here we take advantage of the fact that vitrophyres—that is, the original glassy material formed on initial quenching of the deposits—may hold invaluable kinetic constraints on the emplacement dynamics.

Rheologically (or kinetically) the eruption and welding of ignimbrites requires three crossings of the glass transition ($T_g$) (Gottsmann and Dingwell, 2001a). Magma needs to: (1) fragment to ash during ascent and eruption fountaining, (2) liquefy and relax during transport, deposition, agglutination and welding at high temperature, and lastly (3) quench by cooling into the glassy state. The structure of the glass frozen in at $T_g$ reflects kinetic information from the point at which structural relaxation ceases (Dingwell and Webb, 1990). The cooling path dependence of $T_g$ and its role in forming glass thus holds information as to the cooling rate of magma, which is experimentally accessible via geospeedometric approaches (Gottsmann and Dingwell, 2001a; Gottsmann et al., 2004). Here, we combine rheological measurements, chemical analysis, glass geospeedometry and a 1D analytical thermo-mechanical model to assess the physico-chemical evolution and, specifically, to constrain the duration of eruption, deposition and cooling of a high-grade ignimbrite in the Snake River Plain (USA).

GREY’S LANDING IGNIMBRITE

The Late Miocene Grey’s Landing member is a high-grade ignimbrite resulting from Snake-River (SR)-type volcanism (Branney et al., 2008), preserved in the Rogerson Graben and inferred to originate several tens of kilometers to the east, on the southern margin of the Twin Falls eruptive center (Figure 1; Cathey and Nash, 2004; Andrews and Branney, 2011). Detailed studies of the ignimbrite have described a 5–75-m thick deposit unit divided into a (1) basal vitrophyre, overlain by (2) a thick, parataxitic, lithoidal core, (3) a thin upper vitrophyre, and sometimes (4) a non-welded top (Andrews et al., 2008; Andrews and Branney, 2011). The vitrophyres are generally continuous and do not exhibit evidence of any large-scale folding or brittle failure resulting from vigorous post-depositional flow (c.f., Branney et al., 2004). The basal and upper vitrophyres consist of a poorly sorted mixture of densely-welded (~0.075 and 0.095 pore volume fraction, respectively) glass shards with mildly eutaxitic fabrics and containing small amounts (~5%) of microlites of andesine, pigeonite, augite, hypersthene, and titanomagnetite (Figure 2). Previous geothermobarometry study on pigeonite-augite crystal pairs suggests pre-eruptive magmatic temperatures ranging between 900 and 1050°C (Andrews et al., 2008)—a temperature range constrained by setting pressure to 5 kbar (Cathey and Nash, 2004), based on isotopic analysis for these high-temperature, low $d^{18}$O rhyolite work (Leeman et al., 2008).

GEOCHEMICAL ANALYSIS

On the basis of bulk whole-rock analysis, the Grey’s Landing ignimbrite comprises an anhydrous, metaluminous rhyolite with 72.5 wt% SiO$_2$ (Table 1; Andrews et al., 2008). The chemical composition of the interstitial glass and, importantly, its volatile content provide some first order constraints on its melt rheology. The glass, as measured by electron probe micro-analysis, is also a metaluminous rhyolite and here we constrain its rheology using the model for hydrous, metaluminous melts (Hess and Dingwell, 1996).

We quantified the volatile content of the glass using a simultaneous differential scanning calorimeter/thermal gravimetric analyzer (DSC-TGA) with exsolved gas analysis (mass spectrometer, MS). Standard procedures for DSC-TGA analysis were followed (Newman et al., 1986; Denton et al., 2009) with two heating cycles to 1250°C at 5°C min$^{-1}$.

During the first heating cycle the sample lost 2.61 wt%, indicative of its total volatile content (Figure 3). Insignificant weight loss during the second heating cycle bears testimony to the near-complete nature of the degassing occurring during the first heating cycle. Degassing occurred over a broad temperature range from 200 to 500°C. The rate of weight loss peaked at 298°C and corresponded well with the peak H$_2$O count recorded in the MS, indicating that the weight loss was dominated by water, although CO$_2$, F, and Cl loss also occurred (at concentrations carrying minor rheological impacts on silicate liquids, Hess and Dingwell, 1996; Morizet et al., 2007). Using the relative magnitudes of the MS species counts water is estimated to comprise 92% of the volatiles lost, giving an estimated water content of 2.39 wt%.

Water loss predominantly occurred at low temperatures, indicating that molecular water concentrations greatly exceeded those of hydroxyl (Denton et al., 2009, 2012). The water speciation is therefore typical of low, significantly sub-magmatic temperatures (e.g., Stolper, 1989). We propose that molecular water entered the sample pore space at temperatures <500°C during post-depositional hydration (Denton et al., 2009), due to the high solubility, yet low diffusivity of water in silicate glass at low temperature (Zhang et al., 2007), and that little disassociated magmatic water was present. An important implication is that a trivial amount of magmatic volatiles were present in the melt as it last crossed the glass transition, suggesting that degassing was near-complete in this explosive super-eruption.

ROCK-MAGNETIC SIGNATURE

We employed a magnetic measurements variable field translation balance (VFTB) to measure the Isothermal Remanent Magnetisation (IRM), backfield, hysteresis and thermomagnetic curves to help identify the magnetomineralogy and domain state in the basal vitrophyre as well as constrain the conditions at which the sample hydrated (Figure 4). For this purpose, small cylinders of vitrophyre (6 mm diameter and 5 mm high) were subjected to varying applied magnetic fields and the resulting
FIGURE 1 | Extent of the Grey’s Landing ignimbrite (shaded in gray) in the Rogerson Gragen, Snake River Plain, Idaho, USA.

FIGURE 2 | Photomicrograph of the Grey’s Landing basal vitrophyre showing a dense agglomerate of eutaxitic glass shards with moderate aspect ratio (3:5). The glass hosts a small amount of plagioclase (Pl), pyroxene (Px), oxide (in white) and pores.

Table 1 | Chemical composition of the Grey’s Landing basal vitrophyre.

| Oxides     | Glass 1  | Glass 2  | Bulk     |
|------------|----------|----------|----------|
| SiO₂       | 79.088   | 78.876   | 72.543   |
| Al₂O₃      | 11.965   | 12.050   | 11.812   |
| Na₂O       | 1.882    | 1.754    | 2.995    |
| K₂O        | 5.897    | 5.934    | 5.174    |
| MgO        | 0.000    | 0.006    | 0.239    |
| CaO        | 0.295    | 0.264    | 1.448    |
| TiO₂       | 0.330    | 0.357    | 0.499    |
| Fe₂O₃      | 0.442    | 0.487    | 3.501    |
| MnO        | 0.005    | 0.027    | 0.064    |
| P₂O₅       | 0.019    | 0.035    | 0.082    |
| Cl          | 0.030    | 0.027    | –        |
| LOI        | –        | –        | 1.911    |
| Total      | 99.932   | 99.826   | 100.267  |

The interstitial glass was analyzed with a CAMECA SX100 electron microprobe, using a defocused beam [15 kV, 20 nA scanning box mode (102 µm²)] and the calibration standards: Na, albite; K, orthoclase; v12, rhyolite. Bulk rock analysis were obtained by XRF (Andrews et al., 2008).
magnetisation was measured both before (hysteresis) and after (IRM and backfield) switching the field off. Subsequently, the samples were placed in a constant field of 240 mT and heated in air to 700°C and then cooled back down to room temperature. The dataset was analyzed using the RockMagAnalyzer software by Leonhardt (2006). We find a good consistency between all samples. IRM and backfield curves (Figures 4A, B) show evidence for both low and (minor) high coercivity phases with saturation not fully achieved by 800 mT. The hysteresis loop (Figure 4C) also shows some “wasp-waisting” (Tauxe et al., 1996) suggesting that phases with very different coercivity are present within the sample. The bulk hysteresis properties give a remanent magnetization/ saturation magnetization (Mr/Ms) of 0.19 and the coercivity of remanence/coercive force (Bcr/Bc) of 5.6 placing it within the pseudo single-domain (PSD) region of the Day et al. (1977) plot close to the single-/multi-domain (SD/MD) mixing line of Dunlop (2002). All thermomagnetic heating and cooling curves (undertaken in air) show at least two Curie Temperatures in the basal vitrophyre (Figure 4D). The first is at 210–230°C, likely representing an Fe-Ti oxide (potentially a near-primary titanohaematite), and the second at 550–580°C indicating near-stoichiometric magnetite.

The difference in shape of the cooling and heating curves suggests that during laboratory heating, the Fe-Ti oxide grains were variably oxidized to have more distributed, higher Curie Temperatures and higher saturation magnetisation values. The results suggest that this rock was originally subject to oxidation of its primary magnetic phases at elevated temperatures but that it cooled too quickly to achieve equilibrium. We do not find evidence for (titanio) maghaemite which suggests the oxidation was confined to temperatures at least above 800 mT. (C) Hysteresis loop, used for estimating a Mr/Ms of 0.19 and a Bcr/Bc of 5.6; (D) Thermomagnetic Curves (undertaken in air) show at least two Curie Temperatures at 210–230°C, and at 550–580°C.
200°C. Similarly, the presence of a Ti-rich phase and its readiness to alter under laboratory heating supports limited (or no) primary oxidation occurring above 700°C. This iron oxidation temperature constraint is concordant with the observation that sample dehydration reaction around <500°C (Figure 3) may reflect a late, post-magmatic hydration phase by meteoric water.

**GEOSPEEDOMETRY**

A differential scanning calorimeter (DSC) was used to quantify the glass transition temperature and to derive the natural cooling rate of the interstitial glass. 55.99 mg of crushed glass were selected, washed with acetone and oven-dried at 110°C for 60 min. Specific heat capacities of the glass shards (placed in a lidded platinum crucible) were measured in argon atmosphere in a DSC calibrated against a single crystal sapphire of similar mass in identical measurement conditions. The samples were treated to 950°C in successive heating/cooling runs at matching cooling and heating rates of 10/10, 10/10, 20/20, 15/15, 10/10, and 5/5°C.min⁻¹ (details of the method and volcanology applicability can be found in Scherer, 1990; Wilding et al., 1995, 1996; Gottsmann and Dingwell, 2001a, b). Geospeedometry requires fitting the raw heat capacity curve of the first heating cycle (from original samples with an unknown, natural cooling rate) by modeling the heat capacity peaks associated with the glass transition of each cooling/heating cycle of a known rate.

During the first heating run, we observe a broad peak in heat capacity at 250–600°C and a narrow peak associated with the transition of the glass to a supercooled melt at 800–920°C, which peaks at 870°C (Figure 5A). We attribute the low-temperature DSC peak to devolatilisation of molecular water, as it coincides well with the temperature range of degassing in TGA measurements. In the following runs, the low-temperature peak is absent and only the glass transition peak remains, although the measured heat capacities progressively diminish. Extrapolation of the glass transition peaks can be used to estimate the natural cooling rate of a liquid as it vitrifies. Note that it remains possible that the accuracy of geospeedometric estimates may be jeopardized if post-depositional hydration were to modify the structure originally trapped in at the glass transition; no rheological studies yet account for such a phenomenon. Here, application of geospeedometry provides us with an estimate of the cooling rates of the basal vitrophyre at ~0.1°C.min⁻¹ (Figure 5B).

**“LAVA-LIKE” RHEOLOGY**

The viscosity of the Grey’s Landing melt was investigated through dilatometric measurements. Cylindrical disks with heights and diameters of 8 mm were placed in the dilatometer and heated at a rate of 10°C.min⁻¹ to various temperatures (870, 900, 930, 960°C). Once the sample was thermally equilibrated after 10 min, a small indenter was released onto the sample and the rate of indentation was used to calculate the temperature (T) dependence of the viscosity (η₀ in Pa·s; Figure 6). In the narrow temperature span the measurements constrain the viscosity to:

\[
\log_{10}(\eta_0) = \frac{9601}{T - 195.7} - 3.545
\]

This temperature dependence of the viscosity is in agreement with the description of a low water content (0.2–0.25 wt.%), metaluminous rhyolite (Hess and Dingwell, 1996).

The strain rate dependence of the Grey’s Landing melt rheology was investigated using a high-temperature (<1300°C), high-pressure (1–300 kN) uniaxial press equipped with acoustic sensors (see Hess et al., 2007; Lavallée et al., 2008, for detail on the technique). Large cylindrical cores with heights and diameters of 50 and 25 mm, respectively, were prepared and a set of three 2-mm wide holes was drilled along the sample axis to permit the insertion of thermocouples. The sample was placed between the pistons of the press, heated up to given temperatures (900, 920, 940°C) and thermally equilibrated for 9 h. Subsequently, a series of loads of 8.0, 16.0, and 24.0 kN (equivalent to stresses of 15.5, 31.0, and 46.5 MPa) were consecutively applied, the piston displacement was monitored, and the rheology was evaluated.
During the experiments there were no detectable acoustic emissions that would be expected to accompany microcracking of the sample; this implies that all strain was viscously accommodated (e.g., Lavallée et al., 2008). Moreover, we monitored no temperature increase, which would have arisen from any significant viscous heating. Analysis of high-resolution (20 μm) neutron tomographic images was used to further investigate the deformation mechanism (Online Supplementary Material). Even in samples with up to 33% strain, we observed viscous deformation (e.g., Lavallée et al., 2008). The observed Newtonian rheology indicates that the basal vitrophyre behaved as a Newtonian fluid which does not undergo significant viscous heating within the applied stress conditions.

An equation developed for parallel plate measurements (Gent, 1960) was used to calculate the apparent suspension viscosities \( \eta \):

\[
\eta = \frac{2\pi Ph^5}{3V \frac{dh}{dt} (2\pi h^3 + V)}
\]  

where \( V \) is the initial volume of sample (m\(^3\)), \( h \) is the height (m), and \( dh/dt \) is the rate of length change (m.s\(^{-1}\)). [Note that we use the term apparent viscosity to describe the general rheology of the suspension consisting of liquids, crystals, pores (see Lavallée et al., 2007) without reference to the stress - strain rate description of the rheology]. The calculated viscosities are in reasonably good agreement with the viscosities obtained by dilatometry (Figure 6). We observed no stress (or strain rate) dependence of the apparent viscosity, which could have been associated with an abundance of crystals (Lavallée et al., 2007), with the deformation of pores between glass shards (Quane and Russell, 2005b),

viscous heating (Hess et al., 2008) or failure (Lavallée et al., 2008). The observed Newtonian rheology indicates that the basal vitrophyre behaved as coherent viscous liquid typical of low-crystallinity, low-porosity lavas once the pores collapsed to the observed end-fraction.

**TIMESCALE OF THE GREY’S LANDING IGNIMBRITE ERUPTION**

The combination of geothermometry, based on equilibrium crystallization temperature of the mineral assemblage, and geospeedometry, based on glass transition analysis in the welded glass shards, is used to constrain the timescale of eruption and emplacement of the Grey’s Landing ignimbrite. Pre-eruptive temperature estimates of 900–1050°C (Andrews et al., 2008) and a measured glass transition temperature of 870°C allow for a maximum temperature window for cooling of the material during eruption, transport and deposition of 30–180°C. A complementary rheological study has proposed that viscous energy dissipation during intense shearing may have increased the temperature conditions for rheomorphism by tens of degrees and perhaps up to 250°C (Robert et al., 2013). It remains that upon cooling, the basal vitrophyre cooled through the glass transition at a rate of ∼0.1°C.min\(^{-1}\).

We apply an analytical approach combining a 1D model for conductive heat transfer with a viscoelastic mechanical model to account for progressive changes in heat conductivity in a porous magma undergoing compaction. Our assumptions are (1) that the ignimbrite was deposited instantaneously and (2) that it experienced no deformation during aggradation. Our model is a simplification of nature as it has been constrained that the deposition of pyroclastic density currents results from progressive aggradation (e.g., Branney and Kokelaar, 1992), yet we assume that deposition is extremely rapid and that deposition temperature may be relatively uniform, in order to use current mechanical models. Thus, the starting conditions of the model are homogeneous initial temperature and total porosity. The heat transfer is governed by conservation of energy following the 1D heat equation:

\[
\frac{\partial T}{\partial t} = \kappa \frac{\partial^2 T}{\partial z^2}
\]

for which \( z \) represents the vertical distance (m) perpendicular to the surface of the deposit and \( \kappa \) the thermal diffusivity (m\(^2\).s\(^{-1}\)) of the porous material. The classical definition of the thermal conductivity assumes a pore-free material and, here, we refine this definition to consider the insulation provided by the porosity of the material (e.g., Connor et al., 1997):

\[
\kappa = \frac{k}{\rho C_p (1 - \phi) + \rho' C'_{p} \phi}
\]

where \( k \) is the thermal conductivity (W.m\(^{-1}\).K\(^{-1}\)), \( \phi \) the total porosity, \( \rho \) and \( C_p \) the skeletal density (kg.m\(^{-3}\)) and specific heat capacity (J.kg\(^{-1}\).K\(^{-1}\)) of the solid respectively, and \( \rho' \) and \( C'_{p} \) the density and the specific heat capacity of the pore fluid (Table 2). The pore fluid pressure is assumed to be atmospheric, which is
Table 2 | Initial thermal parameters.

| Variable | Value | Melt/Glass | Country rock | Pore fluid |
|----------|-------|------------|--------------|------------|
| $k_0$ (m².s⁻¹) | – | 1.59 | 1.59 | 0.025 |
| $\rho$ (kg.m⁻³) | – | 2900 | 2330 | 1.275 |
| $C_p$ (J.kg⁻¹.K⁻¹) | – | 1000 | 1000 | 1007 |
| $\phi_i$ | 0.5 | – | – | – |
| $\lambda$ | 3.6 | – | – | – |

reasonable considering the lack of confinement to prevent expansion. The thermal conductivity is also a function of the porosity of the material considered. Some empirical models have been proposed to relate the thermal conductivity of a porous rock to its pore-free thermal conductivity $k_0$ (Bagdassarov and Dingwell, 1994):

$$k = k_0 \left( \frac{1 - \phi}{1 + \phi} \right)$$ (5)

Analytical solution of Equation (3) for geological systems has most commonly been achieved by assuming self-similarity of solutions (Carslaw and Jaeger, 1947). Assuming homogeneous initial temperature, Carslaw and Jaeger (1959) treat the problem of a cooling magma body in contact with a county rock at $z = 0$ and which solidifies at and below its solids temperature. In our case we use the glass transition temperature in place of the solidus. A derived solution of Equation (3) for the temperature profile in the melt is as follows:

$$T_{melt} (z, t) = T_i + \frac{T_g - T_i}{\text{erfc} \left( \frac{\lambda}{\sqrt{2k_m t}} \right)} \text{erfc} \left( \frac{z}{2\sqrt{k_m t}} \right)$$ (6)

where $T_i$ and $T_g$ are the initial and the glass transition temperature (K) of melt respectively, $k_m$ and $\lambda$ are the thermal diffusivity of the melt and the glass respectively, and $\lambda$ a non-defined thermal constant. Carslaw and Jaeger (1959) have shown that the temperature profile in the solid portion, here, glass, can be described by the following equation:

$$T_{glass} (z, t) = \frac{T_g}{k_g \sqrt{k_c} + k_c \sqrt{k_g} \text{erf} (\lambda)} \left[ k_g \sqrt{k_c} + k_c \sqrt{k_g} \text{erf} \left( \frac{z}{2\sqrt{k_g t}} \right) \right]$$ (7)

where $k_c$ is the thermal diffusivity of the underlying country rock. The solidification surface occurs following $z_{glass}(t) = 2\lambda \sqrt{k_m t}$.

This thermal approach is further combined with a mechanistic and kinetic description of the compaction of the deposited ash (Quane and Russell, 2005b, 2006; Quane et al., 2009). The porosity evolution with stress $\sigma$, viscosity of the material at zero porosity $\eta_0$ and time $t$ can be derived using the empirical equation (Quane et al., 2009):

$$\Delta t = \frac{\eta_0}{\alpha \sigma (1 - \phi_i)} \left[ \exp \left( -\frac{\alpha \phi_i}{1 - \phi} \right) - \exp \left( -\frac{\alpha \phi_i}{1 - \phi} \right) \right]$$ (8)

where

$$\phi (t) = \frac{\beta}{\beta - \alpha}$$ (9)

and

$$\beta = \ln \left( \frac{\alpha \sigma}{\eta_0 (1 - \phi_i)} t + \exp \left( -\frac{\alpha \phi_i}{1 - \phi_i} \right) \right)$$ (10)

Here, $\phi_i$ is the initial total porosity and $\alpha$ an empirical constant. Following Quane et al. (2009) we use $\sigma = 0.78$ for packing of volcanic ash. The stress distribution across the entire deposit is described by the overburden as $\sigma (z) = \rho (1 - \phi)gz$ where $g$ is the gravitational acceleration (m.s⁻²).

This set of Equations (4–10) provides the tools to iterate a thermo-mechanical model describing the feedbacks between compaction via destruction of porosity, temperature (and thus viscosity) and stress upon deposition. Using a set of constrained glass parameters (Table 2), we simulate the progression of compaction as a function of time and initial temperature (Figure 7).

The model results suggest that for the pyroclasts at a stratigraphic height of $z = 0.3$ m to reach the measured $\phi = 0.075$ at $T = T_g$, and a constrained cooling rate of 0.1°C.min⁻¹, a little under 1 h is required. Due to the interplay between cooling and compaction, we can further deduce that ~966°C is the idealized deposition temperature $T_1$ to meet the measured conditions of porosity, stratigraphic position and cooling rate (Figure 8). This compaction time estimate may be faster if syn-depositional shearing (e.g., Robert et al., 2013) were to have achieved higher stresses than the overburden load considered in our model.

The welding timescale calculated here agrees well with the 12–20 min proposed by similar rheological modeling by Robert et al. (2013) but is significantly shorter than the 10–15 h proposed for the Bishop Tuff (Long Valley Caldera, California, USA) by Wilson and Hildreth (1997). In contrast it is orders of magnitude more rapid than the thermo-mechanical constraints on the Bandelier Tuff (Valles Caldera, New-Mexico, USA) estimated at 1–5 days (Quane et al., 2009), the Rattlesnake Tuff estimated at 10 s of days (Riehle et al., 2010), the Bishop Tuff estimated at 10–100 s of days (Wilson and Hildreth, 1997; Sheridan and Wang, 2005; Riehle et al., 2010), and on a rheomorphic phonolitic fallout deposit (Las Cañadas Caldera, Tenerife, Spain) estimated at 25–54 days (Soriano et al., 2002). The study constrains that welding is not, as previously suggested, decoupled from cooling (e.g., Sheridan and Wang, 2005) but rather is synchronous with cooling. Here we demonstrate that welding (i.e., sintering and formation of eutaxitic textures) reflects the temperature-time window in which the erupted products remain in the liquid state (above the glass transition temperature of the glass fraction of the pyroclasts).

The general agreement between the onset temperature of welding (966°C) and the geothermometric constraint (900–1050°C) suggests that little cooling took place during eruption and transport (unless frictional processes contributed in large amounts; e.g., Robert et al., 2013; Lavallée et al., 2014). In this sense, there are strong parallels between large ignimbrites and tuffisites within silicic lava-filled conduits, which exhibit similar dense welding textures (Tuffen et al., 2003). In tuffisites, minimal
cooling occurs between fragmentation and sintering due to isolation from the atmosphere in intrusive pyroclastic channels. The inference is that for large-volume ignimbrites the bulk of the magma is similarly thermally insulated from the atmosphere (Suzuki and Koyaguchi, 2010; Sulpizio et al., 2014), despite degassing to near-atmospheric pressure; a similar insulation has been postulated from examination of ignimbrite emplaced sub-aqueously (Kokelaar and Koniger, 2000). This must reflect minimal entrainment of surrounding fluids (air or water) during pyroclastic fountaining and flow. It may also reflect a wide source vent (e.g., Legros et al., 2000). Cooling of pyroclasts may therefore be largely prevented until deposition (e.g., Lesti et al., 2011), thus supporting the view that the thermal history of explosive eruptions and emplacement are decoupled.
CONCLUSION
The experimental and analytical constraints described above help to unravel the timescales of deposition of large-volume high-grade ignimbrites. The narrow temperature window between the residence in the reservoir and the transition to a glass indicates a high discharge rate, rapid post-fragmentation transport and deposition, and rapid agglutination, welding, and rheomorphism. We estimate the timescale of sintering (welding) and rheomorphism of the basal vitrophyre at a little under 1 h and further constrain that deposition and onset of sintering occurred when the ash particles approximated 966°C. Our rheological experiments confirm that, at their original emplacement temperature, the vitrophyres exhibit Newtonian properties at applied stresses up to 46 MPa (corresponding to a 2 km thick deposit). Thus, the use of the term “lava-like” is physically reasonable for describing the rheological properties of the vitrophyres of high-grade ignimbrites; moreover, it suggests that viscous heating may be minimal for such flow unless applied stresses are significantly higher than those exerted by the overburden. Together, rheological and analytical measurements may serve to constrain the temporal and physico-chemical evolution framework of ignimbrite eruptions and, in the case of the Grey’s Landing ignimbrite, support a short timescale of emplacement.

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