History of the mass ejection in K 4-37: from the AGB to the evolved planetary nebula phase

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ABSTRACT
We present narrow-, broad-band, and WISE archive images, and high- and intermediate-resolution long-slit spectra of K 4-37, a planetary nebula that has never been analyzed in detail. Although K 4-37 appears bipolar, the morphokinematical analysis discloses the existence of three distinct axes and additional particular directions in the object, indicating that K 4-37 is a multi-axis planetary nebula that has probably been shaped by several bipolar outflows at different directions. A 4-6 M⊙ main-sequence progenitor is estimated from the derived high nebular He and N abundances, and very high N/O abundance ratio (∼2.32). The general properties are compatible with K 4-37 being a highly evolved planetary nebula located at ∼14 kpc. The WISE image at 22 µm reveals K 4-37 to be surrounded by a large (∼13 × 8 pc²) elliptical detached shell probably related to material ejected from the AGB progenitor. The observed elliptical morphology suggests deformation of an originally spherical AGB shell by the ISM magnetic field or by the influence of a companion. We compare K 4-37 and NGC 6309 and found remarkable similarities in their physical structure but noticeably different chemical abundances that indicate very different progenitor mass. This strongly suggests that, irrespective of the initial mass, their (presumably binary) central stars have shared a very similar mass ejection history.

Key words: planetary nebulae: individual (K 4-37) – interstellar medium: jets and outflows.

1 INTRODUCTION
It is well known that planetary nebulae (PNe) originate from Asymptotic Giant Branch (AGB) and post-AGB stars with low- and intermediate-mass (∝ 8–10 M⊙) main-sequence progenitors once the central star becomes hot enough to photoionize the envelope ejected during the AGB phase. It is also well known that this process, when applied to single star evolution, can hardly explain the dramatic transformation of a spherical AGB envelope into the varied and complex morphologies observed in a noticeable number of PNe (e.g., Balick & Frank 2002).

During many years the formation of PNe has been understood within the Interacting Stellar Wind model (ISW; Kwok, Purton & Fitzgerald 1978; Balick 1987). This model has probed its ability to explain many of the features observed in PNe (Balick & Frank 2002, and references therein). However, multiple, highly collimated, and axisymmetric structures in PNe have always presented difficulties to be explained within the ISW scenario. Nowadays, in addition to wind-wind interaction, it is recognized that the formation of complex PNe requires the action of collimated outflows that distort an originally spherical AGB envelope (Sahai & Trauger 1998). In this context, binary central stars were always though to be determining in the formation of complex PNe (e.g., Morris 1981; Soker & Livio 1994). The importance of binary central stars in PN formation is receiving strong support with the detection of new post-common envelope binary central stars associated to complex PNe (Miszalski et al. 2009; Miszalski 2012; Jones 2016; and references therein). Evolution through a common-envelope provides many of basic ingredients though to be involved in the formation of complex PNe, as accretion disks, highly collimated outflows,
Nowadays, about 3500 PNe are known in the Galaxy (Parker, Bojić & Frew 2016). However, many of them still lack an analysis that allow us to place them within the evolutionary sequence and to carry out comparisons with other PNe, which could provide information to disentangle the possible key processes involved in the formation of the different kinds of PNe. Given the enormous variety of properties (e.g., morphology, kinematics, chemical abundances, physical conditions) exhibited by PNe, increasing the number of well analyzed objects may contribute to shed light on the processes involved in the AGB to PN transition.

K 4-37 (PN G066.9+02.2; \( \alpha(2000.0) = 19^h 51^m 60^s; \delta(2000.0) = +31^\circ 02' 29'' \)) is a PN that has never been analyzed in detail. It was discovered by Kohoutek (1965) and its PN nature can be guessed from the emission line fluxes listed in the Strasbourg ESO Catalog (Acker et al. 1992). According to this catalog, the nebula presents very strong \([\text{N} \text{II}]\) and \([\text{S} \text{II}]\), moderate \([\text{O} \text{III}]\), and absent \([\text{He} \text{II} \lambda 4686] \) emission lines, indicating a very low-excitation PN. Except for these data, information about the characteristics and properties of K 4-37 is lacking in the published literature. The object was imaged by us many years ago in our programs to study compact PNe (e.g., Miranda et al. 1997, 2000, 2001; Vázquez et al. 2002), and it showed a simple and less interesting bipolar morphology. However, the acquisition and analysis of new data, and inspection of the WISE archive have revealed noticeable properties in this PN. In this paper we present the data, analysis, and results that we have obtained for K 4-37.

2 OBSERVATIONS AND RESULTS

2.1 Optical imaging

Narrow-band images of K 4-37 were obtained during 1998 July 7-9 with CAFOS at the Calar Alto Observatory. The detector was LORAL 2k×2k CCD with a plate scale of 0.33 arcsec pixel\(^{-1}\). Three filters were used: H\(\alpha\) (FWHM =
The planetary nebulae K 4-37

The planetary nebulae K 4-37 have been studied extensively due to their interesting morphology and the central star's properties. In this section, we will focus on the analysis of the WISE (Wide-field Infrared Survey Explorer) images of K 4-37 obtained in 2014 and 2016.

**Figure 3.** Grey-scale reproduction of the WISE image at 22 μm (W4) around K 4-37 (arrowed). Grey-levels are linear. North is up, east to the left, and the field of view is 15×15 arcmin². The elliptical ring-like structure is arrowed.

The planetary nebulae K 4-37 have been studied extensively due to their interesting morphology and the central star’s properties. In this section, we will focus on the analysis of the WISE (Wide-field Infrared Survey Explorer) images of K 4-37 obtained in 2014 and 2016.

The WISE images show a noticeable limb-brightening and a knotty structure in the bipolar lobes. Moreover, the northwestern lobe is clearly distorted or broken towards the west where an elongated feature is observed up to ∼7.3 arcsec from the center, which clearly deviates from the lobe geometry. An eastern counterpart cannot be recognized in the southeastern lobe (Fig. 2) but we note that the region along PA ∼90° protrudes and does not follow the lobe geometry. In fact, the southeastern lobe can be traced up to ∼5.7 arcsec from the center along PA ∼90° whereas it extends only ∼4 arcsec at PA ∼180°. The distorted regions subtend an angle of ∼30° as seen from the center. From the images in Fig. 2 two different axes are identified in K 4-37: one along PA ∼40°, defined by the main axis of the lobes and bright torus, and another one along PA ∼270° (or ∼90°), defined by the distortions of the bipolar lobes. Besides, the point-symmetric features suggest additional particular directions in the nebula.

The central star of K 4-37 has never been identified and is neither observed in our narrow-band images. Central stars with V or B magnitudes ≤ 17 mag can be detected in (narrow-band) Hα or [OIII] images with moderate exposure times, which implies that the central star of K 4-37 should be very faint. In an attempt to detect it, we obtained an image of K 4-37 with CAFOS in 2016 May 3 using a Johnson B filter and an exposure time of 1200 s, under seeing conditions of ∼1.5 arcsec. No star can be recognized in our B image close to the center of the object, where the central star could be expected, which would imply a lower limit of ∼20 mag for its B magnitude. On the other hand, it is well known that central stars may be displaced from the nebular center (e.g., Soker 1994; Tweed & Napiwotzki 1994; Soker, Rappaport & Riepea 1998; Chiotellis et al. 2016). We note that the images of K 4-37 show a star at ∼1.7 arcsec from nebular center (Figures 1 and 2). Its spectrum indicates a K-type star (see Section 2.3). A (somewhat speculative) alternative to the non detection of a star at the nebular center could be that the central star and the K-type star constitute a (non-resolved) binary system that has moved since the nebula was formed. If this was the case, the angular distance to the center and the age of the nebula (∼10⁷ yr, Section 3.2) would imply a proper motion of ∼0.17 mas yr⁻¹ for the pair, corresponding to a tangential velocity of ∼11 km s⁻¹ (at a distance of 14 kpc, see Section 3.2). If so, the large distortion of the nebula towards the west, as compared with that towards the east, could be partially due to that motion. In any case, further efforts to detect the central star of K 4-37 would be very valuable.

**2.2 WISE imaging**

To complement our analysis, we have retrieved the images of K 4-37 obtained with the Wide-field Infrared Survey Explorer (WISE) satellite in the four bands: W1 (3.4 μm),
Figure 4. Flux-calibrated spectrum of K 4-37. The left inset shows the spectrum between 4300 and 6400 Å and the right inset in the [N\textsc{ii}] λλ6548,6583 and H\textalpha{} region. [A color version of the figure is available in the online version.]

W2 (4.6 μm), W3 (12 μm), and W4 (22 μm), in a field of 15×15 arcmin\(^2\) centered on the object.

K 4-37 itself is not resolved in the WISE images owing their relatively low spatial resolution (6.1–12 arcsec) and the small size of the object. In addition, the field star observed in the optical images (Fig. 2) is bright at 3.4–22 μm and this star and the nebula are indistinguishable in the WISE images. The more interesting result is observed in the W4 band a reproduction of which is shown in Figure 3. K 4-37 appears embedded in a complex nebular environment in which stands out an elliptical ring-like structure surrounding the optical PN. Emission from the ring-like structure is also observed in the W3 band but more diffuse and fainter than in the W4 one, and is not observed in the W1 and W2 bands (not shown here). The elliptical ring-like structure (hereafter referred to as the 22 μm ring) is open (or very faint) towards the northwest, contains a bright spot towards the southwest, and presents a complex region towards the northeast where it seems to contact an ambient filament. The edge of the 22 μm ring is relatively bright but emission is also detected inside it. The complex northern region makes it difficult to obtain accurately the orientation and major axis of this structure. Nevertheless, its minor axis appears oriented close to PA \(\sim -60^\circ\) and is \(\sim 2\) arcmin in size, its major axis is \(\sim 2.9\)–3.6 arcmin in size as measured at PA 30° (in the following we will adopt a major axis of 3.2 arcmin), while a size of \(\sim 2.4\) arcmin is measured at PAs 75° and 165°. From the image in Fig. 3, an association, and not a superposition chance, between the 22 μm ring and the optical nebula is strongly suggested because the 22 μm ring, the only closed structure observed in the field, is well centered on K 4-37. Nevertheless, the optical nebula seems to be slightly displaced towards the southeast with respect to the possible center of the 22 μm ring, which is difficult to define because of its complex northern region. The large difference in sizes between the optical nebula and the 22 μm ring strongly suggests that the latter should correspond to a much older ejection than that involved in the formation of the main nebula. As we will discuss below (Section 3.3), the 22 μm ring probably represents mass ejected from the AGB progenitor of K 4-37. We note that the detection of this structure at 22 μm suggests dust as origin of its emission.

2.3 Intermediate-resolution long-slit spectroscopy

Intermediate-resolution, long slit-spectra of K 4-37 were obtained on 2008 June 8 with the Boller & Chivens spectrograph mounted on the 2.1 m telescope at the San Pedro Mártil Observatory (OAN-SPM)\(^1\), using the SITe3 CCD (plate scale 24 μm pix\(^{-1}\)), with a 1k×1k pixel array as a detector. We used a 400 lines mm\(^{-1}\) dispersion grating along with a 2.5 arcsec slit width, giving a spectral resolution (FWHM) of \(\sim 6.5\) Å and covering the 4300–7400 Å spectral range. The slit was centered on the nebula and oriented at PA 90°. Four spectra were obtained with an exposure time of 1800 s each. Spectra reduction was carried out following standard pro-

\(^1\) The Observatorio Astronómico Nacional at the Sierra de San Pedro Mártir (OAN-SPM) is operated by the Instituto de Astronomía of the Universidad Nacional Autónoma de México.
Table 2. The IC method of Kingsburgh & Barlow (1984) has and indeed with a relatively strong intensity of about a third
values of $N$ electron temperatures are quite typical of PNe, while the $N/O$ abundance ratio of type I PNe (e.g., Kingsburgh & Barlow 1994). What
served in PNe (see, e.g., Pottasch, Beintema & Feibelman 2000; Akras et al. 2016 and references therein)
Table 1. Dereddened emission line intensities in K 4-37 in units of $I_{\beta}$

| Ion          | $\lambda$ | $f(\lambda)$ | $I(\lambda)$ |
|--------------|-----------|--------------|--------------|
| $H\beta$     | 4340      | 0.129        | 64.5 $\pm$ 5.9 |
| [O iii]      | 4363      | 0.124        | 12.2 $\pm$ 3.7 |
| $He\beta$    | 4686      | 0.042        | 29.9 $\pm$ 2.8 |
| $H\beta$     | 4861      | 0.000        | 100.0 $\pm$ 2.3 |
| [O iii]      | 4959      | 0.024        | 194.5 $\pm$ 3.4 |
| [O iii]      | 5007      | 0.035        | 572.5 $\pm$ 9.5 |
| [N i]        | 5199      | 0.075        | 26.0 $\pm$ 1.1 |
| [N ii]       | 5755      | 0.192        | 24.0 $\pm$ 0.7 |
| $He\beta$    | 5876      | 0.216        | 15.3 $\pm$ 0.6 |
| [O i]        | 6300      | 0.285        | 20.2 $\pm$ 0.6 |
| $S\alpha$    | 6312      | 0.287        | 5.5 $\pm$ 0.4 |
| [O i]        | 6363      | 0.294        | 5.5 $\pm$ 0.3 |
| [N ii]       | 6548      | 0.321        | 465.9 $\pm$ 13.9 |
| $Ho$         | 6563      | 0.323        | 283.9 $\pm$ 8.0 |
| [N ii]       | 6583      | 0.326        | 1414.8 $\pm$ 39.8 |
| $He\beta$    | 6678      | 0.339        | 5.2 $\pm$ 0.3 |
| $S\alpha$    | 6716      | 0.343        | 60.9 $\pm$ 1.8 |
| $S\alpha$    | 6731      | 0.345        | 53.6 $\pm$ 1.6 |
| $He\beta$    | 7065      | 0.383        | 4.8 $\pm$ 0.3 |
| $Ar\beta$    | 7136      | 0.391        | 25.7 $\pm$ 0.9 |
| [O i]        | 7320      | 0.411        | 4.9 $\pm$ 0.3 |
| [O i]        | 7330      | 0.412        | 5.1 $\pm$ 0.3 |

Table 2. Ionic and elemental abundances by number in K 4-37

| Ion          | Abundance |
|--------------|-----------|
| $He^+$       | $(10^{12})$ 12.060 $\pm$ 0.397 |
| $He^{2+}$    | $(10^{12})$ 2.42 $\pm$ 0.22 |
| $O^+$        | $(10^{8})$ 0.26 $\pm$ 0.01 |
| $O^{2+}$     | $(10^{8})$ 0.93 $\pm$ 0.04 |
| $N^+$        | $(10^{7})$ 1.48 $\pm$ 0.02 |
| $N^{2+}$     | $(10^{6})$ 2.61 $\pm$ 0.11 |
| $S^+$        | $(10^{6})$ 2.15 $\pm$ 0.04 |
| $S^{2+}$     | $(10^{6})$ 2.21 $\pm$ 0.05 |
| $Ar^{2+}$    | $(10^{6})$ 8.93 $\pm$ 0.64 |
| $He/H$       | 0.145 $\pm$ 0.005 |
| $O/H$        | $(10^{6})$ 2.72 $\pm$ 0.06 |
| $N/H$        | $(10^{6})$ 6.31 $\pm$ 0.36 |
| $Ar/H$       | $(10^{6})$ 3.55 $\pm$ 0.79 |
| $S/H$        | $(10^{5})$ 1.25 $\pm$ 0.07 |
2.4 High-resolution long-slit spectroscopy

High-dispersion optical spectra were obtained with the Manchester Echelle Spectrometer (Meaburn et al. 2003) and the 2.1 m (f/7.5) telescope at the OAN-SPM Observatory during 2004 July 29–30. A SiteCCD with 1k×1k pixels was used as detector. The slit length is 6.5 arcmin and its width was set to 150 µm (2 arcsec). A 2×2 binning was used, leading to a spatial scale of 0.66 arcsec pixel$^{-1}$ and a spectral scale of 0.1 Å pixel$^{-1}$. This spectrograph has no cross dispersion, consequently, a ∆λ = 90 Å bandwidth filter was used to isolate the 8th order covering the spectral range that includes the Hα and [N II]λ6548,6583 emission lines. Spectra were obtained with the slit centered across the center of the nebula and oriented at PAs −40° and +90°. Exposure time for each spectrum was 1200 s. The spectra were wavelength calibrated with a Th-Ar arc lamp to an accuracy of ±1 km s$^{-1}$. The FWHM of the arc lamp emission lines was measured to be ≃ 12 km s$^{-1}$ that corresponds to the achieved spectral resolution. Seeing was ∼2 arcsec during the observations. Reduction of the spectra was carried out with standard routines in the IRAF package.

Figure 5 presents position-velocity (PV) maps of the [N II]λ6583 emission line at the two observed PAs. From these high-resolution spectra, the systemic velocity of K 4-37 was measured by co-adding 2.4 arcsec around the central position of the emission line features observed at each PA, and finding the central radial velocity of the resulting line profile. The estimates for the systemic velocity in both spectra and from the Hα and [N II]λλ6548,6583 emission lines are consistent with each other after heliocentric and LSR corrections, and its mean value is $V_{HEL} = -23.7 ± 1.5$ km s$^{-1}$ ($V_{LSR} = -5.3 ± 1.5$ km s$^{-1}$).

The [NII] emission feature in the PV maps (Fig. 5) is dominated by two intensity maxima that correspond to the equatorial ring. The PV map at PA −40° shows two velocity components at each spatial position, as expected from a bipolar shell. The velocity splitting is small and varies between ∼22 and ∼30 km s$^{-1}$. At PA 90° velocity splitting is clearly observed around the center of the line feature but is difficult to recognize at larger angular distances. The long-slit spectrum at PA 90° covers the distorted region towards the west (Fig. 2). In fact, the [NII] emission feature in the PV map at PA 90° is much more extended towards the west than towards the east, in consonance with the images (Fig. 2). If the western nebular regions have been distorted, as the images show, its kinematics may have been distorted, too, which may explain the lack of velocity splitting, as expected from a bipolar shell.

To extract more information from the PV maps, we used the tool SHAPE (Steffen et al. 2011) to find the morphokinematic parameters that are able to reproduce simultaneously the observed morphology and PV maps. It should be emphasized that we did not try to reproduce with SHAPE all the observed features in the PV maps and image in detail as, e.g., changes of intensity (point-symmetric regions, bright knots), (spatial and velocity) widths of the features, and distortions of the structures. Rather, we try to reproduce the variation of the radial velocity (two components) as a function of the spatial position, as observed in the PV maps, and the basic shape (projected contour) of the bipolar lobes and torus, as observed in the image. In Figure 6 we show the deconvolved Hα+[N II] image and [N II] PV maps of K 4-37 together with the results of SHAPE assuming a thin bipolar shell with a homologous expansion velocity law, i.e., expansion velocity ($V_{exp}$) proportional to the radius (r) at each point of the nebula [$V_{exp}(r) = K \times r$] and narrow slits (1 arcsec) at PAs −40° and 90° (but see below).

The equatorial torus is quite well reproduced with a circular structure of 1.9 arcsec in radius, expansion velocity of 15.3 km s$^{-1}$, and a tilt for its axis of 45° with respect to the plane of the sky (red colour in Figure 6). These parameters imply K ∼8.0 km s$^{-2}$ arcsec$^{-1}$. When we applied this law to the bipolar lobes, we found that their kinematics cannot be reproduced satisfactorily, even though their morphology can be reproduced acceptably (blue colour in Figure 6). It is clear that the kinematics of the bipolar lobes predicted assuming homologous expansion results to be very different from the observed one. Firstly, we have considered whether a slit width of 2 arcsec (as we used for the long-slit spectra, see above) could have an effect on the resulting shape of the blue lines in Figure 6. However, the use of a 2 arcsec slit produces virtually the same results as shown in Figure 6, except that the blue lines become slightly thicker inwards as a result of including nebular regions at both sides of the main axis, which have somewhat lower radial velocities than along the main axis. Other effects, as, e.g., smoothing due to seeing, may also increase the thickness of the blue lines but the apparent tilt of these lines in the PV maps remains unchanged. Then, we have modified (one by one and simultaneously) several parameters involved in the analysis (e.g., size of the polar axis, polar expansion velocity, inclination angle of the polar axis, in all cases also with a 2 arcsec slit width) and our conclusion is that reproducing the morphokinematics of the bipolar lobes requires that the main axis of the lobes is not perpendicular to the plane of the torus, and, in addition, that a non-homologous expansion law should be considered. In Fig. 6 (green colour) we also show the morphology and kinematics expected if the main axis of the lobes is tilted by 20° with respect to the plane of the sky, the semi-major axis is 5.3 arcsec, and the polar expansion velocity is 34 km s$^{-1}$. These parameters provide a much more acceptable reproduction of the kinematics observed in the PV maps and keep an acceptable representation of the morphology of the lobes as well. They also imply K ∼6.4 km s$^{-1}$ arcsec$^{-1}$ for the bipolar lobes, that is sensibly different from that obtained for the equatorial torus. We note that the western region of the PV map at PA +90° is difficult to reproduce (Fig. 6), and emission is observed at higher redshifted radial velocities than the predicted ones. This suggests that the distorted region could be more tilted than the axis of the lobes (i.e., >20° with respect to the plane of the sky), but a more precise determination would require spectra at higher spectral and spatial resolution. We have also checked the range of tilt angles capable to provide a reasonable reproduction of the observed morphokinematics and found that the deduced tilt angles are correct within ±3° for the axis of the bipolar lobes and ±1.5° for the axis of the torus. These uncertainties are much smaller than the difference in tilt angles (~25°), supporting that the difference is real. Finally, we note that the expansion velocities obtained in K 4-37 (~15–35 km s$^{-1}$), are noticeable lower than those observed in other bipolar PNe.

The morphokinematical analysis has disclosed the pres-
Figure 5. Grey-scale and contours position-velocity maps of the \([\text{N} \text{II}] \lambda 6583\) emission line at the two observed PAs (upper right). The grey levels and contours are logarithmic. Spatial and velocity scales are identical in both panels and indicated in the left one.

Figure 6. Grey-scale H\(\alpha + \text{[N II]}\) deconvolved image (left), and grey-scale and contours position-velocity (PV) maps of the \([\text{N} \text{II}] \lambda 6584\) emission line (middle and right). The grey levels and contours are logarithmic. The orientation of the long slits are plotted on the image (slit width not to scale), and the PV maps contain information about the orientation, and spatial and velocity scales the latter two being identical in the middle and right panels. Overimposed on the panels are the results of shape: red color corresponds to the equatorial torus, blue color to the bipolar lobes assuming homologous expansion velocity, and green color to the bipolar lobes assuming non-homologous expansion velocity and an inclination angle for the bipolar lobes different from that of the torus (see text for details). [A colour version of this figure is available in the online version.]

ence of two different axes where only one is observed in the images as a the main bipolar axis. By chance, due to our line of sight, the axes of the torus and bipolar lobes appear aligned on the plane of the sky at about the same PA (≈ 40°), but they present different tilts with respect to the observer (see also Section 3.4 for the case of NGC 6309). These two axes add to the axes of the distortions of the bipolar lobes and the orientation of the point-symmetric regions, which are all different from each other. According to these results, K 4-37 may be better classified as a multi-axis PN rather than among bipolar PNe with a single axis.

The non-homologous expansion found in K 4-37 is worth mentioning. The idea that PNe expand in an homologous manner has prevailed during long time mainly due to the fact that a simple homologous expansion velocity law is able to reproduce the observed PV maps of many PNe in a quite satisfactory manner. Nevertheless, PNe are known in which such a law is unable to reproduce the observed PV maps (e.g., Miranda et al. 1999; Steffen, García-Segura & Koning 2009; Steffen et al. 2013; Bermúdez 2015). In these cases, the action of collimated outflows on the shell and interaction between the stellar wind and an inhomogeneous shell have been invoked to explain the non-homologous expansion (see references above). In this context, the formation of the bipolar lobes of K 4-37 seems to require a focussed wind/outflow along a direction that is not perpendicular to the equatorial bright torus. In PNe, these kind of outflows are usually related to binary central stars. The possibility that at least in some PNe, non-homologous expansion could be suggesting a binary central star should be investigated.

From the morphokinematic parameters we obtain kinematical ages of \(~590 \times D[\text{kpc}]\) yr and \(~740 \times D[\text{kpc}]\) yr for the
torus and bipolar lobes, respectively, that seem to imply that the formation of the bipolar lobes has preceded that of the torus. However, given the uncertainties involved in the analysis, we will consider a mean value of $665 \times D [{\text{kpc}}]/{\text{yr}}$ for the kinematical age of K 4-37. As of the 22 $\mu$m ring, if we assume a constant expansion velocity of 15 km s$^{-1}$ (typical of AGB envelopes), its kinematical age is $\sim 3.1 \times 10^4 \times D [{\text{kpc}}]/{\text{yr}}$, much larger than that of the bipolar nebula.

3 DISCUSSION

3.1 The evolutionary status of K 4-37

If the global properties derived in the previous sections are considered, K 4-37 seems to find its right place among the group of highly evolved PNe recently analyzed by Akars et al. (2016, hereafter AK16). Tables 3 and 4 in AK16 and Tables 1 and 2 in this work show the common properties. These PNe, including K 4-37, show very strong [N ii] and [S ii] emissions that place them in the lower-left region of the diagram $\log(\text{H} \alpha + \text{[N ii]})$ versus $\log(\text{H} \beta + \text{[S ii]})$ (see Fig. 9 in AK16). AK16 call the attention to the presence of unusually strong [N ii], [O i] emission lines in their sample of highly evolved PNe, which suggest a contribution of shock excitation (see also Akras & Gonçalves 2016). K 4-37 presents [N ii] and [O i] to H$\beta$ line intensity ratios comparable to those in the sample by AK16, and, therefore, shocks are probably contributing to the line emission. These PNe also present high He and N abundances, and high N/O abundance ratios, indicating progenitors of $\sim 5 M_\odot$, and very low electron densities (AK16; see Section 2.3). To these common characteristics, we add the presence of a relatively strong He i$\lambda$4686 nebular emission (He i$\lambda$4686/H$\beta$ $\sim 0.2$–$0.5$; Table 1; AK16 and references therein). This is probably related to the high effective temperature of their central stars (AK16). Although the central star of K 4-37 has not been detected, its presumable faintness and relatively strong He i$\lambda$4686 nebular emission suggest that it could be of low luminosity and high effective temperature, as those in the sample analyzed by AK16.

3.2 The distance of K 4-37

We have obtained a kinematical age of $665 \times D [{\text{kpc}}]/{\text{yr}}$ for K 4-37 that depends on its distance (Section 2.4). Although the distance is unknown, the resulting kinematical age should be compatible with K 4-37 being a highly evolved PN. If, as a first approximation, we assume a kinematical age of $>10000 \text{yr}$ as representative of a highly evolved PN (see AK16), the distance to K 4-37 is $>15 \text{kpc}$. A more confident distance can be obtained by using the recent surface brightness–radius relationship by Frew, Parker & Bojić (2016), the observed Hα flux and $c(\text{H} \beta)$ (Table 2), and a mean nebular radius of ~6.8 arcsec. With these values, the distance is ~14 kpc and, consequently, the kinematical age is $\sim 9300 \text{yr}$, compatible with a highly evolved PN.

For 14 kpc, the size of the nebula is $\sim 0.72 \times 0.26 \text{pc}^2$, very much smaller than the size of the 22 $\mu$m ring that amounts $\sim 13 \times 8 \text{pc}^2$ and whose kinematical age is of $\sim 4.3 \times 10^4 \text{yr}$. Taking into account the age of the nebula and that a 4–6 $M_\odot$ star traverses the post-AGB phase in $\lesssim 100 \text{yr}$ (Blöcker 1995), the kinematical age of the 22 $\mu$m ring places its formation in the AGB phase of the progenitor of K 4-37.

Finally, the low expansion velocities in K 4-37 suggest that the shell might have been decelerated in the course of the evolution. If this was the case, the “true” kinematical age of K 4-37 would be $<665 \times D [{\text{kpc}}]/{\text{yr}}$, and 14 kpc could be a lower limit to the distance to make compatible the kinematical age of K 4-37 with its evolved nature. In any case, it seems to be clear that K 4-37 should be located at a relatively large distance.

3.3 Mass ejection history in K 4-37

Our data analysis has shown that K 4-37 should be classified as a multi-axis PNe. In addition, a very large elliptical structure has been found at 22 $\mu$m surrounded the optical nebula, which probably corresponds to mass ejected in the AGB phase of the progenitor of K 4-37. These findings provide information about the formation history of K 4-37.

According to the properties described in the previous sections, the 22 $\mu$m ring probably is a detached shell related to mass ejected during the AGB phase. The emission detected inside the ring indicates that it is filled with material while the bright edge traces the site of interaction between the AGB ejections and the ISM (e.g., Villaver, García-Segura & Manchado 2002; Schöier, Lindqvist & Oflofsson 2005; Mattsson, Höfner & Herwig 2007). Detached shells are observed in many AGB and post-AGB stars (e.g., Speck, Meixner & Knapp 2000; Cox et al. 2012; and references therein). To the best of our knowledge, the 22 $\mu$m ring in K 4-37 is the largest one of this kind of shells, only comparable to that around R CrB (size $\sim 8.7 \text{pc}$, Gillett et al. 1997), and much larger than those around AGB stars (sizes $\sim 0.4$–$0.8 \text{pc}$, e.g., Oflofsson et al. 2000; Cox et al. 2012), and post-AGB stars as, e.g., AFGL2688 and CRL618 with sizes of $\sim 4$ and $\sim 6.6 \text{pc}$, respectively (Speck et al. 2000). Although the evolution of the these shells may be complex (e.g., Villaver et al. 2002), detached shells around AGB and post-AGB stars could be expected to grow noticeably when the (possible) associated future PNe reach a highly evolved phase.

The elliptical morphology of the 22 $\mu$m ring contradicts the spherical mass ejection that is expected to dominate during the AGB phase (e.g., Oflofsson et al. 2000; Kerschbaum et al. 2010). It is interesting to speculate about the origin of this morphology. Deformation of an original spherical AGB shell by the own interaction with the ISM can be ruled out because of the very peculiar ISM structure required to create a well defined elliptical ring. The 22 $\mu$m ring has some resemblance with the “eye-type” shells observed around some AGB stars (Cox et al. 2012). “Eye-type” shells have been modeled as deformation of an AGB spherical shell by the ISM magnetic field (van Marle, Cox & Decin 2015) and a similar model could be applicable to the 22 $\mu$m ring. Alternatively, a companion could flatten the (spherical) envelope of an AGB star (Maunon, Huggins & Cheung 2013) resulting in an oblated shell. Molecular line observations of the 22 $\mu$m ring are required to study its kinematics, and to derive its 3D structure and properties.

The formation of K 4-37 itself fits well into the usual scenario in which several bipolar outflows have shaped the nebula (Sahai & Trauger 1998). As observed in many PNe, the
bipolar outflows should have been ejected at different directions and their collimation degree has also changed; a poor collimated outflow seems to be involved in the formation of the bipolar lobes while more focused outflows could be related to the distortions of the lobes and point-symmetric regions. Our data do not allow us to establish a possible time sequence in the generation of the various outflows, although the bipolar lobes may be ascribed to a major ejection event.

### 3.4 Comparison of K 4-37 and NGC 6309

Among multi-axis PNe, we found striking morphological similarities between K 4-37 and NGC 6309, a PN with a bright equatorial torus and two pairs of bipolar lobes at different directions (Vázquez et al. 2008; Rubio et al. 2015). Knotty and point-symmetric structures can be recognized in the lobes as well as distortions in one of the pairs of NGC 6309, characteristics that are present in K 4-37 as well. Interestingly, the two pairs of bipolar lobes and the torus of NGC 6309 seem to be tilted with respect to the observer by the same amount (Vázquez et al. 2008; Rubio et al. 2015). This implies that if NGC 6309 was observed from a line of sight perpendicular to the current one, it would appear as a “simple” bipolar PN, with a pair of bipolar lobes and an equatorial torus sharing a single main axis, and resembling the images of K 4-37; in this case, only a morphokinematical analysis of NGC 6309 would be able to reveal the existence of two pairs of lobes and different orientations of the structures. Moreover, a spherical halo surrounds NGC 6309 and evidence exists for a large shell with a size of $\sim 1.5 \times 10^3$ pc and a kinematical age of $\sim 1.5 \times 10^7$ yr (Rubio et al. 2015). This comparison strongly suggests that the central stars of K 4-37 and NGC 6309 share a similar mass ejection history. In particular, the specific processes involved in the shaping of the multi-axis structure should have been very similar in both PNe.

Some differences can be noticed between K 4-37 and NGC 6309. In particular, the electron density in NGC 6309 (1400-4000 cm$^{-3}$, Vázquez et al. 2008) does not indicate a particularly young or a highly evolved PN, in consonance with its kinematical age of $\sim 4000$ yr (Vázquez et al. 2008; Rubio et al. 2015) that suggests a moderately young/evolving PN. Probably K 4-37 and NGC 6309 are in a different evolutionary stage within PN evolution, being K 4-37 in a more advanced one.

However, the most interesting difference between K 4-37 and NGC 6309 is observed in their chemical abundances that are listed in Table 3. Although He seems to be slightly over-abundant in NGC 6309, N may be deficient, and the N/O abundance ratio is very low. Albeit multi-axis, NGC 6309 is not a type I PN (Vázquez et al. 2008). Chemical abundances in PNe are primarily related to the initial mass of the progenitor. Therefore, K 4-37 and NGC 6309 should have evolved from progenitors of very different mass. The chemical abundances in NGC 6309 (Table 3) and the models by Karakas (2010) suggest an initial mass of $\sim 1-1.2 M_\odot$ for its progenitor, while 4-6 $M_\odot$ were estimated in the case of K 4-37 (see above). Vázquez et al. (2008) noticed that the existence of the multi-axis structure of NGC 6309 strongly contrasts with the idea that these kind of PNe should be associated with intermediate-mass progenitors (e.g., Corradi & Schwarz 1995). The striking structural similarities between K 4-37 and NGC 6309 strengthen this conclusion: stars with very different initial mass have been able to shape very similar PNe at the end of their lives. The complexity of K 4-37 and NGC 6309 is compatible with that expected from binary central stars and, in particular, from those having evolved through a common envelope phase. It is known that post-common envelope binary central stars tend to be associated with complex PNe that often show multiple structures and/or signs of collimated/focused outflows (Miszalski et al. 2009; Aller et al. 2015). In NGC 6309, evidence (but not conclusive yet) exists for a possible F3V companion, as suggested by the near-IR excess observed towards its central star (Douchin et al. 2015). In K 4-37 such an evidence does not exist. Nevertheless, given the complexity of the nebula, it is reasonable to propose a binary nature for the central star of K 4-37.

### 4 CONCLUSIONS

We have presented and analyzed narrow- and broadband images, intermediate- and high-resolution spectra, and WISE archive images of K 4-37, a PN not analyzed before. The main conclusions of this work can be summarized as follows.

- K 4-37 appears as a bipolar PN consisting of a bright equatorial torus, two main bipolar lobes, point-symmetric structures and off-axis deformations of the bipolar lobes. Its internal kinematics cannot be reproduced assuming an homologous expansion velocity law. The morphokinematical analysis allows us to disclose the existence of three distinct axes and additional particular directions in K 3-37 that may be classified as a multi-axis PN.
- Very strong $\text{[N II]}$, $\text{[S II]}$ and relatively strong He I emission lines are observed in the nebular spectrum. High He and N abundances, and a very high N/O abundance ratio ($\gtrsim 2.32$) are obtained. A progenitor of $\sim 4-6 M_\odot$ is estimated. The nebula presents a very low electron density indicating a highly evolved PN.
- A distance of $\sim 14$ kpc is estimated for K 4-37, which is compatible with its highly evolved PN nature and a kinematical age of $\sim 10^8$ yr.
- The WISE image at 22$\mu$m reveals K 4-37 to be surrounded by a very large elliptical detached shell with a size of $\sim 13 \times 8$ pc$^2$ and a kinematical age of $\sim 4.3 \times 10^5$ yr. This
shell is probably related to the mass ejected during the AGB phase of the progenitor of K 4-37.

- The elliptical morphology of the detached shell is not compatible with the spherical mass ejection expected in the AGB phase. Deformation of an originally spherical shell by the ISM magnetic field and/or the influence of a companion could explain the peculiar morphology. The formation of the nebula itself is better understood as caused by several focussed outflows at different directions and with different collimation degrees.

- Remarkable morphological similarities exist between K 4-37 and NGC 6309. However, chemical abundances largely differ in both PNe, indicating progenitors of very different initial mass. These results suggest that the initial mass of the progenitor has not played a crucial role in shaping these two PNe but their formation can be better attributed to a similar mass loss history of their central stars that, given the complexity of both PNe, are probably binary.

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