A hybrid imputation approach for microarray missing value estimation

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Abstract

Background: Missing data is an inevitable phenomenon in gene expression microarray experiments due to instrument failure or human error. It has a negative impact on performance of downstream analysis. Technically, most existing approaches suffer from this prevalent problem. Imputation is one of the frequently used methods for processing missing data. Actually many developments have been achieved in the research on estimating missing values. The challenging task is how to improve imputation accuracy for data with a large missing rate.

Methods: In this paper, induced by the thought of collaborative training, we propose a novel hybrid imputation method, called Recursive Mutual Imputation (RMI). Specifically, RMI exploits global correlation information and local structure in the data, captured by two popular methods, Bayesian Principal Component Analysis (BPCA) and Local Least Squares (LLS), respectively. Mutual strategy is implemented by sharing the estimated data sequences at each recursive process. Meanwhile, we consider the imputation sequence based on the number of missing entries in the target gene. Furthermore, a weight based integrated method is utilized in the final assembling step.

Results: We evaluate RMI with three state-of-art algorithms (BPCA, LLS, Iterated Local Least Squares imputation (ItLLS)) on four publicly available microarray datasets. Experimental results clearly demonstrate that RMI significantly outperforms comparative methods in terms of Normalized Root Mean Square Error (NRMSE), especially for datasets with large missing rates and less complete genes.

Conclusions: It is noted that our proposed hybrid imputation approach incorporates both global and local information of microarray genes, which achieves lower NRMSE values against to any single approach only. Besides, this study highlights the need for considering the imputing sequence of missing entries for imputation methods.
mode of gene attributes [9]. Although this method requires quite a few computations, it may import error for the analysis of the studied mechanism. Actually, this approach would produce lots of same values, which is somewhat disagree with the situation of reality. The third method is to impute the missing values by their estimated values based on the observed information in the microarray dataset. The latest studies have shown that this method has strong adaptability and can obtain better imputation accuracy. Therefore, several methodologies have been developed in recent years [10].

Algorithms on imputing missing values can be classified into four categories [11,12]: global approach, local approach, hybrid approach and knowledge assisted approach. Each of them has its own characteristics. We will give a brief introduction on these approaches.

Global approach estimates missing values based on global correlation information extracted from the entire data matrix [12]. The frequently used global approaches include Singular Value Decomposition (SVD) [13] and Bayesian Principal Component Analysis (BPCA). These methods is characterized by the ability of capturing global correlation information to restore the missing values. But they ignore the local structure hidden in the data. Details of BPCA will be presented in later sections.

Correspondingly, local approach uses the potential local information to estimate the missing values, such as Local Least Squares (LLS) and Weighted K-Nearest Neighbor imputation (WKNN) [14]. LLS estimates missing values using a multiple regression model [11] based on K-nearest neighboring genes with respect to the target gene. Currently, several LLS variants have been proposed to improve algorithm performance in different aspects, such as Iterated Local Least Squares imputation (ItrLLS) [15], sequential Local Least Squares (slLS) [16], weighted Local least squares (wLLS) [17]. Obviously, this type of method could estimate missing values accurately if the data matrix contains rich local structure. In other words, algorithms would obtain poor imputation performance when the missing values have strong correlation with the global information rather than local structure. In the next section, a short review of LLS and ItrLLS will be given.

Hybrid approach, apparently, is derived by combined both global and local correlations of the data matrix. Hence, using the hybrid method may achieve higher imputation performance than a single type approach only. LinCmb [18] and EMDI [19] are two typical hybrid approaches.

Knowledge assisted approach integrates domain knowledge or external information into the imputation process, which may significantly improve the imputation accuracy [12], such as Fuzzy C-Means clustering (FCM) [20] and Projection Onto Convex Sets (POCS) [21]. Wherein, FCM used gene ontology annotation as external information to process missing values imputation. However, the priori knowledge is difficult to extract and its veracity is hard to control. Thus, this problem causes poor applicability with these methods for data imputation.

Recently, many novel imputation algorithms have been developed, such as bicluster-based impute (BIC) [22], bicluster-based Least Square (bi-iLS) [23] and bicluster-based Bayesian Principal Component Analysis (bi-BPCA) [11]. Although they properly utilize data local structure and global correlation information inspired by bicluster algorithm, and a novel framework for missing value estimation is also designed, they still just use them separately without considering the advantage of their combination. Besides, most methods estimate missing values without considering the imputation sequence among incomplete genes. Since incomplete genes that have less missing entries might be recovered more accurately than those with more. The successful design of an estimation method for missing values depends mainly on making full use of the observed information. Thus the question is, how to build models using the different information and, more importantly, how the different methods can strengthen each other. Therefore, it is important to develop a strategy which could use the observed information fully for restoring the missing expression gene values.

In this paper, induced the thought of semi-supervised learning [24] with collaborative training, we propose a novel hybrid imputation method, called Recursive Mutual Imputation (RMI). In the field of machine learning and data mining, we always expect to collect a large amount of labeled data to build a powerful model. But obtaining large labeled data is time consuming and not practical for some fields, especially medical field. Yet, large unlabeled samples are often easy to obtain, making semi-supervised learning methods attractive. Moreover, semi-supervised learning can strengthen the model trained by labeled data through exploiting general knowledge among unlabeled samples. Co-training paradigm, one of a popular used semi-supervised method, is proposed by Blum and Mitchell [25]. It trains two classifiers with sufficient and redundant restrictions, respectively. But in reality, it is not easy to meet those two restrictions. Thus, in contrast to standard co-training configuration, CO-training REGressors (COREG) [26] has a broad applicability as no sufficient and redundant restrictions needed. COREG involves two classifiers, and the core idea of its training process is to select the confident labeled instances from dataset labeled by one learner, and then put them into another learner training set. Inspired by the idea of COREG, for a microarray dataset with a large missing rate, we treat the complete and incomplete genes as labeled and unlabeled examples correspondingly. Then, mutual imputation strategy is designed to
share both global and local information extracted by two different types of imputation methods. To make full use of those information, an recursive imputation for data sequence is developed to improve all estimation results gradually. In our framework, Bayesian Principal Component Analysis (BPCA) and Local Least Squares (LLS) are introduced as our global and local approaches. Therefore, RMI is a hybrid imputation method, and has several distinguished advantages over other methods for restoring the missing expression gene values. Firstly, RMI aims to build a recursive mutual process by assembling two single methods, BPCA and LLS, which can exploits global correlation information and local structure in the missing dataset as full as possible. Secondly, it considers the genes that have less missing entries should be estimated firstly, which can improve the performance of estimation results for genes with more missing entries. Furthermore, a novel weight-based ensemble method is applied to RMI method. Experimental results conducted on several real-world datasets prove the effectiveness of the recursive mutual strategy, even in the case of larger missing rates and less complete genes.

The remainder of the paper is organized as follows. Section 2 reviews BPCA, LLS and ItrLLS approaches. Section 3 describes the proposed algorithm in detail. We presents the experimental results in Section 4. Finally, Section 5 concludes the work.

Review on BPCA, LLS and ItrLLS

Bayesian principal component analysis

BPCA [1] method is performed by three steps in the processes of missing value estimation, as follows: 1) Principal Component (PC) regression, 2) Bayesian estimation, and 3) an Expectation-Maximization (EM)-like repetitive algorithm. In detail, the following example is taken to explain how BPCA works. BPCA regards d-dimensional gene expression vectors y as a linear combination of principal axis vectors wl (1 ≤ l ≤ K, and K < d):

\[ y = \sum_{l=1}^{K} x_l u_l + \varepsilon, \]

where \( x_l \) are called factor scores, \( \varepsilon \) denotes the residual error. The \( l \)th principal axis vector \( u_l = \sqrt{\lambda_l} \mu_l \), where \( \lambda_l \) and \( \mu_l \) denote the \( l \)th eigenvalue and the corresponding eigenvector of the covariance matrix \( S \) for the data set \( Y \). The principal axis vectors \( W = (W^{obs}, W^{miss}) \), where \( W^{obs} \) denote the observed part in the data, and \( W^{miss} \) denote the miss part. If the number \( K \) is given, the factor scores \( x = (x_1, x_2, \ldots, x_K) \) for the expression vector \( y \) can be obtained by minimizing the residual error over the observed data set \( y^{obs} \).

\[ err = ||y^{obs} - W^{obs} x||^2. \]

Then, the missing value in the expression vector \( y \) can be estimated by:

\[ y^{miss} = W^{miss} x. \]

The parameter \( W \) is unknown beforehand in the above procedure. BPCA use a probabilistic model, which is called probabilistic PCA (PPCA). Meanwhile, the model is based on the assumption that the residual error \( \varepsilon \) and the factor scores \( x \) obey normal distributions, as follows:

\[ p(x) = N_K(x|0, I_K), \]

\[ p(\varepsilon) = N_d(\varepsilon|0, (1/\tau) I_d), \]

where \( I_K \) is a (K × K) identity matrix and \( \tau \) is a scalar inverse variance of \( \varepsilon \). \( NK(x|u, \sigma) \) denotes a K-dimensional normal distribution for \( x \), whose mean and covariance are \( u \) and \( \sigma \), respectively. BPCA assumes \( Y = (Y^{obs}, Y^{mis}) \), where \( Y^{obs} \) and \( Y^{mis} \) denote observed part and the missing part. The variational Bayes algorithm [27] is used to estimate the posterior distribution of the parameter \( \theta = \{ W, u, \tau \} \) and \( Y^{mis} \) simultaneously. The value of \( K \) is \( d - 1 \) as default.

Local least squares

Two steps are included in the local least squares imputation procedure [2]: 1) selecting k genes based on Pearson correlation coefficients or Euclidean distance; 2) regression and estimation. Without loss of generality, let \( Y \in R^{m×d} \) denote the expression matrix consisting of \( m \) genes and \( n \) conditions, and the expression value of the \( j \)th gene in the \( j \)th condition is present as \( g_{ij} \). Here we assume the target gene \( g_t \) has missing values at the first \( z \) positions. As the following presents, there are \( k \) coherent genes \( (g_{1t}, g_{2t}, \ldots, g_{kt}) \) for \( g_t \) in matrix \( G \):

\[
\begin{pmatrix}
\mathbf{g}_{1t} \\
\mathbf{g}_{2t} \\
\vdots \\
\mathbf{g}_{kt}
\end{pmatrix}
= \begin{pmatrix}
\mathbf{g}_{1x} w^T \\
\mathbf{g}_{2x} w^T \\
\vdots \\
\mathbf{g}_{kx} w^T
\end{pmatrix} B_{kx} A_{kx(n-z)}
\]

where \( B \) denotes the \( z \) columns in the \( k \) coherent genes corresponding to the \( z \) missing positions of the target gene \( g_t \) and matrix \( A \) denotes the \( n-z \) columns in the \( k \) coherent genes corresponding to the \( n-z \) non-missing positions. \( w^T \) consists of the non-missing positions of \( g_t \). The \( k \)-dimensional coefficient vector \( X \) is regarded as a least squares problem with \( \lambda^T \) and \( w \), that is present as follow:

\[ X = \arg\min_{\lambda} |A^T X - w|^2, \]
Then the \( z \) missing values in the target gene \( g_e \) are estimated by a linear combination of \( B^T \) and \( X \):

\[
g_{i xp}^T = B^T X = B^T (A^T)^\dagger w,\]

where \( (A^T)^\dagger \) denotes the pseudoinverse of \( A^T \). All the missing values in the matrix can be recovered according to the same procedure. Also LLS uses an artificial method to estimate the proper \( k \) mentioned above. In detail, for each target gene, the missing value is replaced by the row average at first. Secondly, a certain number of known entries are removed randomly to create the artificial missing matrix and save the true expression values. Then, LLS is performed on the artificial matrix using every value of \( k \) ranging from 1 to the total number of genes in the matrix. The imputation quality, measured by Normalized Root Mean Square Error (NRMSE) can be calculated once the pseudo missing values are estimated with every \( k \) value. Note that we know the true expression value for each of the pseudo missing value. Finally, the parameter \( k \) is set to the value corresponding to the best imputation quality.

**Iterated local least squares imputation**

Iterated Local Least Squares imputation (ItrLLS) [15] method, one of LLS-derived methods, improves LLS method from two aspects. Firstly, the way of selecting coherent genes in ItrLLS is different from LLS. In LLS, the \( k \) coherent genes are selected as \( k \) nearest neighboring genes. The \( k \) value is fixed for all target genes after the \( k \) is selected at the artificial stage. While in ItrLLS, the number of coherent genes for target genes is not a fixed number. In practice, ItrLLS defines a distance threshold selecting the coherent gene, and the threshold \( \theta \) is set as times the average distance to the target gene. Where \( \theta \) denotes the distance ratio, which is chosen from a range \([0.5, 1.5]\) with an increment 0.1 in the default setting. Secondly, ItrLLS uses iterative strategy. At each iteration, the estimated results from the last iteration is used to re-select coherent genes for every target gene with the same distance ratio, and then applies LLS method to re-estimate the missing values. The number of iterations is 5 as default.

**Recursive mutual imputation**

To some extent, the single imputation method mentioned above works well in estimating missing values. They utilize local structure or global correlation information in the matrix properly. However, using a single type of usual imputation method may achieves less estimation accuracy than the hybrid method. Recently, several studies have shown that the performance of estimation algorithms is seriously constrained by the correlation information and structure in the data matrix [12,28].

In this paper, we propose a novel hybrid imputation method using recursive mutual strategy, called RMI. RMI aims to build a recursive mutual process by assembling two single methods, which could provide more accurate estimation. Two frequently-used methods, BPCA and LLS, are chosen as our baseline imputation algorithms. Since BPCA and LLS are able to capture global correlation information and local structure in the microarray matrix, respectively.

Below we describe the algorithm in detail. Let \( C \) and \( M \) denote complete genes set and incomplete genes set, extracted from the whole matrix \( D \) respectively. At the initial stage, the incomplete matrix \( M \) is divided into \( p \) parts, \( M = (m_{11}, m_{21}...m_{p})^T \), where \( m_i \) includes all genes with \( i \) missing entries, \( p \) is equal to the max number of missing entries. For example, for a matrix with 100 incomplete genes and 10 experiments, all genes that have one missing entries are selected as the gene group \( m_1 \). Apparently, all genes that have two missing entries are selected as group \( m_2 \), and the rest group can be formed in the same way. The \( p \) value might be less than 10 according to the attribute length of microarray data.

Generally, RMI consists of three major steps: two complete gene subsets construction; recursive mutual imputation and estimation results ensemble. Below we describe them in detail.

**Two complete gene subsets construction**

The first step is to construct two complete genes subset, \( C_1 \) and \( C_2 \). As we discussed above, using the more observed information, the more accurate the estimation results. BPCA and LLS can be applied on the whole missing matrix \( G \) at the initial stage. Then, we obtain complete matrix \( G_{bPCA} \) and \( G_{LLS} \). It is not proper to make \( C_1 \) or \( C_2 \) using all genes in \( G_{bPCA} \) and \( G_{LLS} \), since they contain the genes with so many estimated value, which can induce more error. If \( C_1 \) and \( C_2 \) are both set to \( C \), there would less observed information be used, which conflicts with our original view. Here, we set \( C_1 \) by the part of genes in \( G_{bPCA} \) that have less than \( p \) missing entries in the original matrix \( G \). Similarly, \( C_2 \) includes \( C \) and part of genes in \( G_{LLS} \) corresponding to the genes that have less than \( p \) missing entries in \( G \).

**Recursive mutual strategy**

In the recursive mutual process, each subset can use information from each other for \( C_1 \) and \( C_2 \). We consider that incomplete genes should be recovered in the sequence of the size of \( i \), which means RMI uses tactics to recover genes that have less missing entries firstly. In the process of semi-supervised co-training, a key step is to select the confident labeled instances from dataset labeled by one learner, and then put them into another learner training set. They can take respective advantages
to improve the estimation results of each other in this way. In every iteration of RMI, the complete genes \( m_{i\text{b pca}} \) taken out from \( C_{\text{b pca}} \) are regarded as confident genes, then we put them into complete genes set \( C2 \) which would be used in the next iteration of LLS imputation, where \( C_{\text{b pca}} \) and \( C_{\text{lls}} \) denote the imputed results by BPCA and LLS respectively. Correspondingly, \( m_{i\text{lls}} \) taken out from \( C_{\text{lls}} \) should be added into complete genes set \( C1 \) in the next iteration of BPCA imputation. Following that, data imputation would stop until all missing entries in \( M \) are recovered. Note that RMI uses the complete genes’ results from the last iteration.

At the end of RMI, the final complete matrix \( G_{im} \) should be constructed by \( C1 \) and \( C2 \). We assemble the results using different weights for \( C1 \) and \( C2 \). The question is how to determine their weight. In the following, we define a novel confidence measure that suits our imputation model. Confidence in the imputation can be defined as the acceptance of imputation model to all estimation results. We consider that recursive mutual imputation tends to improve their accuracy as the amount of data over the observed entries grows. Actually, how well the estimator works directly depends on the number of observed entries in the missing gene and the correlation information between conditions. Based on this idea, we propose a simple definition for the confidence of each missing entry. For example, the target gene \( g_t \) contains missing entries \( g_t^{\text{obs}} \) and observing entries \( g_t^{\text{mis}} \). \( g_t^{\text{obs}} \) denotes one missing entry in \( g_t^{\text{mis}} \), at the \( i \)th position. The confidence of \( g_t^{\text{obs}} \) in \( C1 \) can be calculated by the following equation:

\[
CON(g_t^{\text{obs}}) = \frac{1}{d_i \cdot \text{reg} - \text{error}(g_t^{\text{obs}})}
\]

where \( d_i \) denotes the mean distance between \( g_t^{\text{obs}} \) and its \( k \) nearest genes in \( C1 \). \( \text{reg, error}(g_t^{\text{obs}}) \) denotes the linear regression error, in which the \( i \)th position is the variable and the other positions in \( g_t^{\text{obs}} \) are variables. Note that these calculations are all based on the complete genes \( C1 \) or \( C2 \).

Assembling the results
The confidence matrix \( CON(M_{\text{b pca}}) \) and \( CON(M_{\text{lls}}) \), corresponding to \( C1 \) and \( C2 \), can be obtained, according to the way we described above. The final step is to assemble the estimation results \( C1 \) and \( C2 \). Here the confidences can be used as the assembling weights, as following:

\[
w_{ij}^{\text{b pca}} = \frac{CON(M_{\text{b pca}})_{ij}}{CON(M_{\text{b pca}})_{ij} + CON(M_{\text{lls}})_{ij}}
\]

\[
w_{ij}^{\text{lls}} = 1 - w_{ij}^{\text{b pca}}
\]

\[
C_{im}^{ij} = w_{ij}^{\text{b pca}} \cdot C1_{ij} + w_{ij}^{\text{lls}} \cdot C2_{ij},
\]

where \( i \) and \( j \) denote the missing positions in \( G \). Algorithm 1 gives the algorithm framework.

Algorithm 1 RMI
Input:
The missing matrix \( G_{im \times n} \) includes the complete genes set \( C \) and the incomplete genes set \( M \).
Here \( M = (m_1, m_2, ..., m_p)^T \).
Output:
The complete matrix \( G_{im} \)

Step 1: Constructing two complete genes subsets;

1: Two complete matrix \( G_{\text{b pca}} \) and \( G_{\text{lls}} \) can be obtained by using BPCA and LLS methods, respectively. The complete subset \( C1 \) is constructed from \( G_{\text{b pca}} \). For each gene in \( C1 \), it has more than 1 and less than \( p/2 \) missing entries in the original matrix \( G \). Similarly, The complete subset \( C2 \) is constructed from \( G_{\text{lls}} \).

Step 2: Recursive mutual strategy;

2: for \( i = 1, 2, ..., p \) do
3: For each missing entries in the target gene \( g_t \) in \( m_i \), obtain the confidences \( CON_{\text{b pca}}(g_t) \) and \( CON_{\text{lls}}(g_t) \) by Eq:

\[
CON(g_t) = \frac{1}{d_i \cdot \text{reg} - \text{error}(g_t^{\text{obs}})}
\]

4: Note that \( CON_{\text{b pca}}(g_t) \) is calculated based on \( C1 \cup C \), and \( CON_{\text{lls}}(g_t) \) based on \( C2 \cup C \).
5: end for
6: Recover the missing entries in \( m_i \) based on \( C1 \cup C \) using BPCA method, denoted \( m_{i\text{b pca}} \).
7: Recover the missing entries in \( m_i \) based on \( C2 \cup C \) using LLS method, denoted \( m_{i\text{lls}} \).
8: Update: \( C1 = C1 \cup m_{i\text{lls}} \); \( C2 = C2 \cup m_{i\text{b pca}} \).

Step 3: Assembling the results;

9: \( G_{im} = \text{Assemble}(C1, C2) \cup C \)

Evaluation

Datasets
We used two types of microarray datasets, time series data and non-time series data to illustrate and evaluate
RMI, following some previous studies [1, 2, 15]. Time series (TS) data includes three datasets, and two of them are used for identification of cell cycle-regulated genes of the yeast *Saccharomyces cerevisiae* (http://genome-www.stanford.edu/cellcycle/) [29]. The tab delimited data file contains three parts: the Alpha-part, cdc-part, and Elu-part. We choose Alpha-part and Elu-part. The first dataset, Alpha, contains 6075 genes in the original file. By removing genes with missing values, it remains 4489 genes and 18 experiments in total. The second dataset contains 5766 complete genes with 14 experiments, named Elu. The third dataset, Ronen, includes two time series in yeast from a study of response to environmental changes (>http://ncbi.nlm.nih.gov/Projects/geo/query/acc.cgi?acc=GSE4158) [30], and is also used in [11] to assess bi-BPCA. The matrix contains 10749 genes in 26 experiments originally. It contains 5342 genes with 26 experiments finally, using the same preprocessing method mentioned in study [11]. The forth dataset, Tacrc, is non-time series dataset and is the cDNA microarray data relevant to human colorectal cancer (CRC) studied in [31]. It contains 758 genes with 50 experiments. The details of these four datasets are shown in Table 1.

### Evaluation measures

The quality of the imputation results is measured by the Normalized Root Mean Square Error (NRMSE), which is described as following

\[
NRMSE = \sqrt{\frac{\sum_{j=1}^{N} (y_j - \hat{y}_j)^2}{N\sigma_y}},
\]

where \( y \) is the real value and \( \hat{y} \) is the value estimated by imputation method, and \( \sigma_y \) is the standard deviation for the real values. \( N \) is equal to the total number of the missing entries. The smaller NRMSE is, the higher estimation accuracy.

### Experimental setup

Three imputation methods, BPCA (http://www.csbio.sjtu.edu.cn/bioinf/EMDI/), LLS (http://webdocs.cs.ualberta.ca/ghlin/src/WebTools/Imputation/) and LL-S (http://www.cs.umn.edu/hskim/tools.html) are selected as comparative methods with RMI. In our experiments, the missing entries are generated based on the general principle. In a first step, the observations with missing values are deleted from the initial gene expression datasets to obtain testing datasets. We consider all complete genes and eliminate genes that have missing entries from the original datasets. Then artificial missing matrices with different missing rate are generated, and all the missing values in a dataset occur randomly. Let \( t \) denotes the complete ratio and \( r \) represents the missing rate. That means about \( t\% \) of the whole genes in \( G \) are randomly selected as complete genes \( C \), while \( r\% \) of entries in the rest genes are removed randomly, denoted \( M \). For example, assuming one matrix contains 1,000 genes, when \( t \) is equal to 0.20, then 200 genes are maintained as complete genes \( C \) and the rest 800 genes make up missing matrix \( M \) with \( r\% \) of entries in \( M \) are removed. In a second step, different imputation methods are applied on these matrices. The evaluation performance between the estimated values and the original real values is calculated with criterion RMSE.

#### Results and analysis

In this work, nine different missing rates \( r \) at 1%–40% with five different complete ratios \( t \) at 5%–25% are simulated in each dataset. Each kind of random case is generated 10 times by varying the set of missing entries to ensure a correct sampling. All the results present in the following figures are the NRMSE average value of 10 results. Figure 1, 2, 3, 4 show the results of four datasets: Alpha, Elu, Ronen and Tacrc. On the whole, it can be seen that RMI achieves the best performance by comparing these results for various missing rates \( r \).

When comparing the three single imputation methods, there is no dominant method suitable for all datasets, different performances are present on the different datasets. Specifically, LLS is powerful for low rates of missing values on Ronen (seen from Figure 3). However, it should be noted that the efficiency of LLS is reduced when the missing rate increases. The same rule can be found from ItrLLS, Figure 3, 4 show us that ItrLLS obtains the lower NRMSE on env and Ronen, while it outperforms BPCA or ItrLLS on the other datasets, Alpha and Elu, especially in the low missing rates cases (seen from Figure 1 and Figure 2). Intuitively, RMI obtains the lower NRMSE on four datasets, which means it can maintain a stable performance, even for dataset with less complete genes and large missing rates. In order to see quantitative performance of RMI, Figure 5, 6, 7, 8 show the NRMSE error between the results of BPCA algorithm or LLS algorithm and RMI. Mathematically, NRMSE error is calculated by the BPCA NRMSE result or LLS NRMSE result minus the RMI NRMSE result on the same dataset. The greater is the \( z \) axis value, the better RMI performs. We can see that RMI method obtains lower N-RMSE than BPCA and LLS on the four datasets. Specifically, compared to BPCA, the NRMSE error averaged on all the test examples is improved by 2.16% on Alpha, 0.91% on Elu, 1.56% on Ronen and 1.71% on Tacrc, with RMI performing the
best among the methods. For LLS, it is improved by 5.18% on Alpha, 6.79% on Elu, 0.77% on Ronen and 1.22% on Tacrc respectively. It can be seen that the worse results for the RMI occur occasionally. However, these just happens in the case of lower missing rates, besides it is hard to make a big gap between the performance of these imputation methods when few missing entries involved.

It should be noteworthy that RMI performs the lower NRMSE error than BPCA with the increase of missing rate $r$ and decrease of complete ratio $t$ (see the left figure of Figure 5, 6, 7, 8). On the contrary, it performs the higher NRMSE error than LLS with the increase of $r$ and decrease of $t$ (see the right figure of Figure 5, 6, 7, 8). This phenomenon is particularly prominent on Elu (see from Figure 6) and Ronen (seen from Figure 7). Because BPCA and LLS can make up for each other via the collaborative strategy in RMI. It also embodies the efficiency of the collaborative strategy. We consider that RMI outperforms comparative methods owing to using not only the local structures but also the global correlation information. Firstly, it aims to build a mutual process by assembling two single methods, BPCA and LLS, which can exploits global correlation information and local structure in the

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**Figure 1** NRMSE on Alpha. The left and the right picture correspond to complete ratio at 0.05 and 0.25 respectively.

**Figure 2** NRMSE on Elu. The left and the right picture correspond to complete ratio at 0.05 and 0.25 respectively.
missing dataset as full as possible. Secondly, it considers the genes that have less missing entries should be estimated firstly, which can improve the performance of estimation for genes with more missing entries. Furthermore, a novel weight-based ensemble method is utilized in it.

**Conclusion**

With the deepening research of DNA microarray, there produces a large number of microarray expression data. Missing values, as an important problem, has been influenced the research progress on this area. Numerous effective single methods have been proposed to estimate the missing values. However, they just uses the global information or local structure in the data matrix, which cannot fully used the observed information. In this study, inspired from collaborative training strategy, we propose a novel imputation method, called RMI. To our best knowledge, this work is the first attempt to focus on using an recursive mutual strategy to estimate missing values. Two frequently used methods BPCA and LLS are incorporated into RMI in order to fully exploit the observed information. In the process of the RMI, we consider the imputation sequence based on the number of missing entries in the target gene. Furthermore, a
Figure 5 NRMSE error on Alpha. NRMSE error between the results of BPCA algorithm (left) or LLS algorithm (right) and RMI on the missing data problem for Alpha.

Figure 6 NRMSE error on Elu. NRMSE error between the results of BPCA algorithm (left) or LLS algorithm (right) and RMI on the missing data problem for Elu.

Figure 7 NRMSE error on Ronen. NRMSE error between the results of BPCA algorithm (left) or LLS algorithm (right) and RMI on the missing data problem for Ronen.
weight-based ensemble method is utilized in the final assembling step. We test four datasets to evaluate the performance of RMI. Various datasets with different missing rates are generated randomly for simulating the reality situation for modeling the real situation of missing matrix, randomly. Experimental results indicate that RMI is powerful and effective to impute missing values. And it is able to perform better performance than comparative methods even when the missing rate is large.

Some further research directions are worth for us to make a deeper study. It includes applying more sophisticated imputation methods in the recursive mutual strategy and to improve our current recursive mutual imputation framework. Another interesting issue is how to choose the right single methods in RMI. Meanwhile, the hybrid strategy is easily extended to develop a multiple hybrid version by using more than two single methods, which is a specific recommendation task.

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Competing interests
The authors declare that they have no competing interests.

Authors’ contributions
H Li and F Shao wrote the paper and done all the computational and analysis works. GZL conceived this paper and proposed the novel idea of RMI. C Zhao and X Wang participated in the design of the experiment. Also GZL and C Zhao revised the paper. All authors read and approved the final manuscript.

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Figure 8 NRMSE error on Tacrc. NRMSE error between the results of BPCA algorithm (left) or LLS algorithm(right) and RMI on the missing data problem for Tacrc.
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