Growth kinetics of Cu$_6$Sn$_5$ intermetallic compound in Cu-liquid Sn interfacial reaction enhanced by electric current

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In this paper, electric currents with the densities of $1.0 \times 10^2$ A/cm$^2$ and $2.0 \times 10^2$ A/cm$^2$ were imposed to the Cu-liquid Sn interfacial reaction at 260 °C and 300 °C with the bonding times from 15 min to 960 min. Unlike the symmetrical growth following a cubic root dependence on time during reflowing, the Cu$_6$Sn$_5$ growth enhanced by solid-liquid electromigration followed a linear relationship with time. The elevated electric current density and reaction temperature could greatly accelerate the growth of Cu$_6$Sn$_5$ and could induce the formation of cellular structures on the surfaces because of the constitutional supercooling effect. A growth kinetics model of Cu$_6$Sn$_5$ based on Cu concentration gradient was presented, in which the dissolution of cathode was proved to be the controlling step. This model indicates that higher current density, higher temperature and larger joint width were in favor of the dissolution of Cu. Finally, the shear strengths of joints consisted of different intermetallic compound microstructures were evaluated. The results showed that the Cu$_6$Sn$_5$-based joint could achieve comparable shear strength with Sn-based joint.

With the rapid multi-functionalization and miniaturization of present electronic devices and the popularization of wide band semiconductors like gallium nitride (GaN) and silicon carbide (SiC), the power density and service temperature increase greatly in current integrated circuits$^{1,2}$. The high temperature electrical interconnection materials are in great demand. However, the traditional high melting point (MP) solder requires higher processing temperature in multiple stacking processes, which may damage the circuits and induce many reliability issues$^3$.

Recently, Cu$_6$Sn$_5$, one of the major Cu-Sn intermetallic compounds (IMCs) in the soldering reaction between Cu substrate and Sn-based solder has drawn a lot of attention as one of the alternatives to traditional Sn-based alloys, for its high melting point, better electromigration resistance, better thermal stability and mechanical properties$^{4-6}$, especially for the low cost and simple processing procedure. However, conventional transient liquid phase (TLP) soldering and solid-liquid interdiffusion (SLID) bonding for full-IMCs joint fabrication are rather time consuming, which will induce serious thermal effect on the reliability of packaging systems$^{7-9}$.

Therefore, many attempts have been tried to shorten the bonding time$^5$, such as increasing soldering temperature or ultrasonic-assisted bonding$^{9,10}$. Recently, a more convenient and effective method of electric current-assisted bonding has been intensively studied, in which solid-liquid electromigration (S-L EM) is utilized to accelerate the bonding process. Huang et al. and Hu et al. have investigated the S-L EM in Cu/Sn-3.5Ag/Cu interconnects, and found that the dissolution rate of the Cu cathode was one order of magnitude higher than that during solid-solid (S-S EM). Liu et al.$^{13}$ imposed an electric current density of $1.44 \times 10^4$ A/cm$^2$ on Cu/Sn/Cu system to fabricate the Cu-Sn interconnections within 180 ms, and achieved a shear strength as high as 67.3 MPa. Ma et al.$^{14}$ has investigated the S-L EM under $0.56 \times 10^3$ A/cm$^2$ in Cu/liquid Sn system by synchrotron radiation real time imaging technology, and found that the Cu$_6$Sn$_5$ layer at the anode grew linearly with the bonding time. Huang et al.$^{15}$ has investigated the size effect on the interfacial reaction, and proposed a concentration gradient controlled (CGC) kinetic model to explain it. However, there are no systematic theories explaining the growth kinetics of Cu$_6$Sn$_5$ in small-size joints under S-L EM system concerning the size effect. Therefore, it is critical to...
investigate and understand the S-L EM process integrally from the dissolution of Cu substrate to the diffusion of Cu atoms in molten Sn, and to the deposition of Cu$_6$Sn$_5$.

This study focuses on the morphology evolution and growth kinetics of Cu$_6$Sn$_5$ in Cu/liquid Sn/Cu system under different electric current densities and temperatures, and takes the Cu concentration gradient into consideration to explain the size effect on the S-L EM system. Furthermore, the correlations between microstructure and shear strength of the Cu-Sn interconnects were studied.

**Results**

**Cross-sectional microstructure evolution.** Figure 1 shows the cross-sectional microstructure evolution of interfacial IMCs in solid-liquid Cu-Sn reaction (without electric current) for various times at 260 °C. Two adjacent thin layers of η-Cu$_6$Sn$_5$ and ε-Cu$_3$Sn formed at both Cu/Sn interfaces. The Cu$_6$Sn$_5$ scallops coarsened continually with bonding time, and the number of scallops decreased accordingly, as shown in Fig. 1a–d. The scallop-type morphology indicates its growth was supply-controlled ripening process, in which Cu$_6$Sn$_5$ grains grew at the expense of their nearest neighbors. At 240 min (Fig. 1e), the relatively larger Cu$_6$Sn$_5$ grains grew from the two original boundary planes were about to contact with each other. The residual Sn gradually ran out and the joint then transformed into full IMC joint, as shown in Fig. 1f. After that, Cu$_3$Sn would keep growing at the expense of Cu$_6$Sn$_5$. The Cu$_6$Sn$_5$ phase still remained in the joint even after 960 min, as shown in Fig. 1f.

Figure 2 shows different microstructures of Cu-Sn IMCs under a current density of 1.0 × 10$^2$ A/cm$^2$ at 260 °C, where the dotted arrow marked by “e” indicates the electron flow direction. The anode Cu$_6$Sn$_5$ grew more rapidly, whereas the growth of cathode Cu$_6$Sn$_5$ was suppressed, showing an obvious polarity effect in 30 min (Fig. 2a,b). After 60 min (Fig. 2c), the tip of anode Cu$_3$Sn$_5$ grains touched the cathode Cu$_6$Sn$_5$, and merged into larger grains. Afterwards, the residual Sn was gradually isolated by Cu-Sn IMCs and the full-Cu$_6$Sn$_5$ joint formed after 120 min (Fig. 2d). After the complete consumption of Sn, the S-L EM transformed into S-S EM, and the dominant reaction within the joints became the formation of Cu$_3$Sn at the expense of Cu$_6$Sn$_5$ (Fig. 2e). Cu was the dominant diffusing species, and the Cu atoms slowly diffused through the Cu$_3$Sn layer and reacted with Cu$_6$Sn$_5$. In this stage, the Cu$_3$Sn layer at either side grew symmetrically in thickness, showing limited sensitivity to electron current. After 480 min, the Cu$_3$Sn phase fully transformed to Cu$_6$Sn$_5$, leaving a honeycomb structure in between.

The EPMA (Electron probe micro-analyzer) analysis was performed to the 15 min sample, and the Cu concentration distribution along the joint was measured (Supplementary Fig. S1). The average Cu concentration dissolved in Sn was 6.86 ± 2.29 at.%, which was higher than the equilibrium Cu concentration at 260 °C shown in phase diagram (~2.401 at.%). Although some details of Cu gradient may be missing during solidification, this result can at least prove that the Cu was oversaturated in liquid Sn.

Figure 1. Morphology evolution in Cu-Sn intermetallic joints at 260 °C for various times: (a) 15 min, (b) 30 min, (c) 60 min, (d) 120 min, (e) 240 min, (f) 960 min.
Another two groups of experiments were performed to further investigate the microstructure evolution under higher electric current density and temperature. When the electric current density increased to $2.0 \times 10^2 \text{ A/cm}^2$ at $260 \, ^\circ\text{C}$, as shown in Supplementary Fig. S2, the precipitation rate of anode Cu$_6$Sn$_5$ increased accordingly, while the growth rate of Cu$_3$Sn had no significant change. One difference in morphology was that there were some cellular structures appearing on the anode Cu$_6$Sn$_5$ grain surfaces, as shown in Fig. S2a and b. The cathode Cu substrates were serrated, whereas the anode Cu substrate was nearly flat, as shown in Fig. S2c and d, which indicates that the cathode was consumed more severely than the anode. Full-Cu$_6$Sn$_5$ joint formed soon after 60 min and full-Cu$_3$Sn joint formed in 360 min, according to Fig. S2c and f.

Keeping the current density constant at $1.0 \times 10^2 \text{ A/cm}^2$ and increasing the temperature to $300 \, ^\circ\text{C}$, the growth rate of both Cu$_6$Sn$_5$ and Cu$_3$Sn increased notably. Similar cellular morphology appeared again to anode Cu$_6$Sn$_5$ grains, which would greatly increase the solid-liquid interfacial surface area for Cu atoms to deposit, as shown in Supplementary Fig. S3. Full-Cu$_6$Sn$_5$ joint formed after 60 min and full-Cu$_3$Sn formed within 360 min, as shown in Fig. S3c and f.

According to the Cu-Sn phase diagram, the liquidus temperature of Cu$_6$Sn$_5$ is above $227 \, ^\circ\text{C}$, while the liquidus temperature of Cu$_3$Sn is above $415 \, ^\circ\text{C}$. Therefore, at $260 \, ^\circ\text{C}$, Cu$_6$Sn$_5$ is the direct reaction product between Cu and liquid Sn, but the Cu$_3$Sn could only be obtained in the solid-state reaction between Cu and Cu$_6$Sn$_5$. As we know, the diffusion coefficient of Cu in the liquid ($D_{\text{Cu}}^{\text{liquid}}$) is several orders higher than that in the solid ($D_{\text{Cu}}^{\text{solid}}$). And the equation of electromigration can be expressed as:

$$j_{\text{Cu}}^{\text{EM}} = C \frac{D_{\text{Cu}}^{\text{liquid}} e^* \bar{z} \rho j}{kT}$$

where, $C$ is the Cu concentration, $T$ is the reaction temperature, $k$ is the Boltzmann constant, $e^*$ is the effective charge of Cu atoms in liquid Sn, $e$ is the electron charge, and $\bar{z}^{e}$ is the product of electrical resistance and current density, representing the electrical field strength. So when the other parameters are constant, the Cu electromigration flux is decided by the diffusion coefficient. Therefore, the electric current can easily influence the Cu diffusion in the liquid rather than in the solid, so the growth of Cu$_6$Sn$_5$ is more sensitive to electric current than Cu$_3$Sn. But the increase of temperature could increase the diffusion coefficient of Cu in liquid and in solid. In summary, increasing electric current density could only accelerate the growth rate of Cu$_6$Sn$_5$, but the increase of temperature could enhance the growth rate of both Cu$_6$Sn$_5$ and Cu$_3$Sn.

Figure 3a shows the change of average Cu$_6$Sn$_5$ thickness with the subtriplicate of time without electric current applied (the details of thickness calculation are presented in the Supplementary Information). The growth of Cu$_6$Sn$_5$ followed a $t^{1/3}$ dependence on time $t$ under the condition of reflowing, which is the characteristic of supply-controlled ripening process. The relationship was then fitted with a line and the ratio of Cu$_6$Sn$_5$ thickness to $t^{1/3}$ was calculated as $2.323 \, \mu\text{m s}^{-1/3}$. Figure 3b shows the thickening kinetics of Cu$_6$Sn$_5$ at the anode in the S-L EM process. It is notable that the Cu$_6$Sn$_5$ phase grew linearly with time before the liquid Sn was totally consumed, indicating a constant deposition rate at the anode. The IMCs were formed even before reaching the corresponding
reflowing temperature because the reactions had already been going on for some time during the heating-up stage. The linear Cu₆Sn₅ thickening kinetics can be presented as:

\[ \Delta X_{\text{Anode}} = \text{const} \cdot t \]  

in which the const is the ratio of anode Cu₆Sn₅ thickness change (\(\Delta X_{\text{Cu₆Sn₅, Anode}}\)) to time (t). The value of const under three different conditions were then calculated as: 0.107 μm/min under 1.0 \(\times\) 10² A/cm², 260 °C; 0.212 μm/min under 2.0 \(\times\) 10² A/cm², 260 °C; and 0.152 μm/min under 1.0 \(\times\) 10² A/cm², 300 °C. The const value nearly doubled when the current density rose to twice the value. Higher temperature could also enhance the growth of anode Cu₆Sn₅. The expression of const will be then confirmed in the discussion part.

**Top-view microstructure evolutions.** Figure 4 shows the three-dimensional morphology of Cu₆Sn₅ grains in the joints reflowed at 260 °C for 15 min, 30 min and 60 min. It can be seen that the Cu₆Sn₅ scallops coarsened with time. Though there were wrinkles appearing on the surfaces, most of the grains maintained the shape of hemisphere and relatively smooth surfaces. According to the ripening theory proposed by K. N. Tu17, if the scallops are assumed to be hemisphere, it follows that the total surface area of the hemispherical scallops of \(2\pi R^2\) is always fixed at twice the base area of \(\pi R^2\), in which R represents the diameter of scallops, independent of the size distribution of the hemispheres. It is an important feature for ripening process which has a constant surface area, rather than a constant volume. It is a non-conservative ripening, and the increase in the total volume of Cu₆Sn₅ relies on the simultaneous supply of Cu atoms in molten solder. Figure 5 shows the Cu₆Sn₅ morphology at 30 min in the other three groups. Figure 5a shows the morphology of Cu₆Sn₅ grains reflowed under 1.0 \(\times\) 10² A/cm² at 260 °C for 30 min, in which more and deeper wrinkles appeared on the surface, showing a tendency of surface area increasing. When the electric current density increased to 2.0 \(\times\) 10² A/cm² (Fig. 5b), intensive cellular structures formed on the surface, indicating the rule of constant-surface area was broken. With the appearance of this structure, the solid-liquid surface area for reaction was nearly doubled, as the cellular structures were also in the shape of hemisphere. Similar phenomenon happened when the ambient temperature was elevated to 300 °C (Fig. 5c), and the effect of temperature on morphology was larger than that of electric current.

**The mechanical properties of the obtained joints.** Shear tests were conducted to evaluate the mechanical properties of the bonded Cu/Sn/Cu joints under different experimental conditions. It can be seen in Fig. 6a that the shear strength were about 40 MPa and kept relatively constant when the reflowing time was less than 60 min. Before 60 min, there was still a lot of Sn in the joints, so the soft Sn phase absorbed most of the stress and deformation. Figure 6b shows the typical cross-sectional fracture morphology at 15 min, indicating that plastic fracture happened within Sn. At 120 min, the shear strength decreased dramatically, as shown in Fig. 6a. Figure 6c shows cross-sectional fracture morphology at 120 min. The Cu₆Sn₅ grains at the anode had combined with the cathode Cu₆Sn₅, forming a Cu₆Sn₅-Sn mixed structure. The Sn phase was divided and constrained by brittle Cu₆Sn₅ phase, and the whole joint could not deform integrally. The mechanical mismatching of the two phase may induce stress concentration to the Cu₆Sn₅ grains. This kind of stress may lead to the fracture along the weak boundary between anode Cu₆Sn₅ and Cu₆Sn₅. When the joints were full of Cu₆Sn₅ phase after 240 min, the shear strength increased because the defects within the joints were reduced, and the Sn ran out totally. The fractures also happened at the boundary between anode Cu₆Sn₅ and Cu₆Sn₅, and the joint achieved the highest shear strength of 44.88 MPa. In short, the Cu₆Sn₅-based joints were able to achieve comparable shear strengths with Sn-based joints as long as the soft phase and defects in them were removed.

**Discussion**

**Growth kinetics of Cu₆Sn₅ in ripening process.** A lot of researchers have investigated the supply-controlled ripening process of Cu₆Sn₅ in the conventional soldering progress, and most of them have proved that its growth follows a \(t^{1/3}\) dependence on time \(t^{1/3}\). This phenomenon can be attributed to the rapid diffusion of Cu.
atoms through channels between Cu$_6$Sn$_5$ grains. Current studies have verified the existence of channels between Cu$_3$Sn and Cu$_6$Sn$_5$ grains\(^\text{20}\). The width $\delta$ of these channels is only about 50 nm, which is much smaller than the average thickness of Cu$_6$Sn$_5$ layers, $X_{\text{Mean}}$. These channels exposed the fresh surface of Cu substrates and served as rapid diffusion paths for Cu atoms to go into the molten solder, whereas the volume diffusion through IMC layer can be ignored. However, with the coarsening of Cu$_6$Sn$_5$ grains, the number and the area of channels decrease, and the supply of Cu atoms reduces. That is the reason why the Cu$_6$Sn$_5$ deposition rate decreases with time rapidly. To reduce the unknown parameters, the distance between the top and the bottom of Cu$_6$Sn$_5$ scallops is replaced by the average thickness of Cu$_6$Sn$_5$ layers, $X_{\text{Mean}}$. The linear relationship between them was proved in previous literature\(^\text{20}\). This process could be approximately described by the equation below based on Fick’s first law\(^\text{17}\):

$$\frac{\partial X_{\text{Mean}}}{\partial t} \approx -D_{\text{Cu}}^\text{channel} \frac{\Delta C}{X_{\text{Mean}}} \left( \frac{\delta}{X_{\text{Mean}}} \right) \frac{V_{\text{Cu}_6\text{Sn}_5}}{6}$$

in which, $D_{\text{Cu}}^\text{channel}$ is the diffusion coefficient through channels, $\Delta C$ is the Cu concentration difference between the top and the bottom of Cu$_6$Sn$_5$ scallops, $V_{\text{Cu}_6\text{Sn}_5}$ is the volume of Cu$_6$Sn$_5$ per mole. Therefore, the average thickness of Cu$_6$Sn$_5$ has a cubic root dependence on time by integrating equation (3):

$$\Delta X_{\text{Mean}} \approx K t^{1/3}$$

in which $K$ is the scale factor, $K = \frac{1}{3}\sqrt{\pi D_{\text{Cu}}^\text{channel} \Delta C V_{\text{Cu}_6\text{Sn}_5}}$. The value of $K$ was calculated as 2.323 $\mu$m/min using the parameters in the Supplementary Table S1. Assuming that the value of $\Delta C$ is similar to the saturation concentration of Cu, the $D_{\text{Cu}}^\text{channel}$ can be calculated as $9.98 \times 10^{-14}$ m$^2$/s, which is similar to the diffusion coefficient in grain boundaries.

**Growth kinetics of Cu$_6$Sn$_5$ in S-L EM.** Under the influence of electric current, the growth kinetics of Cu$_6$Sn$_5$ changes greatly. The electric current changes the distribution of Cu atoms dissolved in molten Sn. In conventional soldering process without electric current, two Cu substrates are the main sources of Cu atoms, as shown in Fig. 7a. Cu concentration distributes systematically in the joint, where the concentration near the substrates is the highest as shown in Fig. 7c. According to Dybko\’s model\(^\text{21}\), the dissolution rate of Cu depends on the concentration in the solid-liquid boundary layer, which can be expressed as:
Figure 6. (a) The shear strength of the joints as a function of bonding time under different conditions, and SEM images of the corresponding fractures under 260 °C, $1.0 \times 10^2$ A/cm$^2$ for (b) 15 min, (c) 120 min, (d) 240 min.

Figure 7. The schematic of Cu flux in molten solder joints under: (a) conventional soldering without electric current (b) solid-liquid electromigration; The schematic of Cu concentration distribution in molten solder joints under: (c) conventional soldering without electric current (d) solid-liquid electromigration.

$$j_{\text{Cu}}^{\text{dissolve}} = D_{\text{Cu}}^{\text{liquid}} \frac{C - C}{w}$$  (5)
where \( J_{\text{Cu,\,dissolve}} \) is the Cu flux of dissolution; \( w \) represents the width of solid-liquid boundary layer, which can be influenced by many external conditions, such as the temperature, convection and so on; \( C \) is the Cu concentration and \( C_s \) is the solubility of Cu in the molten solder at the reaction temperature. When the molten Sn is gradually saturated by Cu, \( \Delta C \) decreases with time, and the dissolution rate of Cu substrate slows down. However, when the electric current is applied to the joint, Cu atoms are able to travel across the joint within a few minutes under electromigration, and a Cu concentration gradient from anode to cathode will be established to balance the electromigration flux. At the cathode, the electric current creates a Cu depletion zone where the Cu concentration is always below its solubility. To maintain the solubility equilibrium, the Cu-Sn IMCs at the cathode keep dissolving into the molten solder. Therefore, the Cu6Sn5 grains at the cathode maintain small size, and the area of channels will not decrease with time. Hence the dissolving rate of cathode will keep constant. At the anode, by contrast, the Cu6Sn5 IMCs deposit rapidly in high Cu concentration and the area of channels shrinks accordingly, and these channels are ultimately blocked by the rapidly thickening IMCs.

The SEM observations also indicated that the Cu atoms in anode IMCs came mostly from the cathode. By observing Figs 2, S2 and S3, we can notice that the Cu substrate at the anode was flat, and continuous layer-type Cu3Sn formed quickly between Cu and Cu6Sn5 after 15 min, which was a good barrier for Cu diffusion. So the Cu substrate at the anode cannot contact with Cu6Sn5 and liquid Sn. By contrast, the Cu substrate at the cathode was rather serrated, and the continuous Cu3Sn layer did not form until the liquid Sn was totally consumed. Recent study has confirmed that the Cu5Sn phase was the reaction product of Cu and Cu6Sn5 at soldering temperature. So we think most of the Cu atoms diffusing from anode had reacted with Cu6Sn5, rather than with Sn. Previous researches have also confirmed that during electromigration, the dissolution of cathode was much more serious than the anode. It’s reasonable to assume that the Cu species in anode Cu6Sn5 came mostly from cathode to simplify the modeling.

So it is obvious that the Cu6Sn5 growth kinetic model in S-L EM will be greatly influenced by the distribution of Cu atoms in molten Sn. To further confirm the expression of const in Eq. (1), the transmission process and the distribution of Cu atoms in the liquid need to be investigated first. There are three main potential rate controlling steps in the growth progress of Cu6Sn5, as shown in Fig. 7(b): (I) the dissolution rate of cathode Cu substrate; (II) the drift rate of Cu atoms under electromigration in the molten solder; (III) the deposition rate of Cu-Sn IMCs at the anode. The ultimate growth rate is determined by the slowest step, as shown in Fig. 7. The numerical value of deposition rate has already been calculated according to the slope of curves in Fig. 3(a). So the flux of Cu for deposition can be calculated accordingly, as shown in Table 1. However, larger deposition rate of 18.4 \( \times \) 10\(^{-4}\) mol/m\(^2\)/s under 250 \( ^\circ\)C, 5.0 \( \times \) 10\(^2\) A/cm\(^2\) had been observed in the experiments performed by Haitao Ma, indicating that the upper limit of deposition rate in our study had not been reached. So the deposition cannot be the rate controlling step either. Although the dissolving rate of cathode was much more serious than the anode, it’s reasonable to assume that the Cu species in anode Cu6Sn5 came mostly from cathode to simplify the modeling.

Table 1. The values of anode Cu6Sn5 deposition rate under different conditions.

| Number | Electric current density \((j)\)/A/cm\(^2\) | Temperature \((T)\)/°C | Joint width \((L)\)/μm | Deposition rate \((J_{\text{Cu,\,deposit}})\)/mol/m\(^2\)/s |
|--------|--------------------------------|--------------------|-----------------|-----------------|
| 1      | 1.0 \( \times \) 10\(^2\)        | 260                | 30              | 0.91 \( \times \) 10\(^{-4}\) |
| 2      | 2.0 \( \times \) 10\(^2\)        | 260                | 30              | 1.79 \( \times \) 10\(^{-4}\) |
| 3      | 1.0 \( \times \) 10\(^2\)        | 300                | 30              | 1.29 \( \times \) 10\(^{-4}\) |
|        | 5.0 \( \times \) 10\(^2\)        | 250                | 400             | 18.4 \( \times \) 10\(^{-4}\) |

According to the analysis above, a balance equation between deposition and drift flux can be described as below:

\[
J_{\text{Cu,\,deposit}} = J_{\text{Cu,\,dissolve}} = J_{\text{Cu,\,EM}} - J_{\text{Cu,\,diffuse}}
\] (6)

\[
J_{\text{Cu,\,deposit}} = -D_{\text{Cu}}^\text{liquid}\frac{dC}{dx} + \frac{D_{\text{Cu}}^\text{liquid}}{kT}e^{\frac{\Delta G_{\text{Cu}}}{kT}}
\] (7)

Given the boundary condition: \( C|_{x=L} = C_s \), in which \( L \) represents the average distance between scallop surfaces at both sides. The distribution of Cu in liquid Sn can be confirmed:

\[
C = C_1 + (C_s - C_1)e^{\frac{\Delta G_{\text{Cu}}}{kT}(x-L)}
\] (8)

in which \( C_1 = \frac{J_{\text{Cu,\,dissolve}}}{D_{\text{Cu}}^\text{liquid}}e^{\frac{\Delta G_{\text{Cu}}}{kT}} \). Since the exponential term is small enough compared with C, the equation (8) could be simplified as a linear relationship:
as depicted by Fig. 7d. So the Cu concentration at the cathode can be expressed as:

\[ C_{\text{cathode}} = C_s - (C_s - C_i) \frac{\bar{z}e\rho jL}{kT} \]  

which means the cathode Cu concentration is always below the saturation concentration, and the concentration difference of them can be expressed as:

\[ \Delta C = C_s - C_{\text{cathode}} = (C_s - C_i) \frac{\bar{z}e\rho jL}{kT} \]  

where \( \bar{z} \) is the area density of the cathode, \( e \) is the electron charge, \( \rho \) is the resistivity of the cathode, \( j \) is the electric current density, and \( L \) is the cathode thickness. The cathode Cu concentration in the above expression is always below the saturation concentration, and the concentration difference of them can be expressed as:

\[ \Delta C = C_s - C_{\text{cathode}} = (C_s - C_i) \frac{\bar{z}e\rho jL}{kT} \]

which increases linearly with the increase of electric current density. Therefore, according to the equations (5) and (6), the dissolution flux and \( \text{const} \) can be expressed as:

\[ \dot{I}_{\text{dissolve}} = \frac{D_{\text{Cu}}}{w} \frac{C_s - C_{\text{cathode}}}{kT} \]

\[ \text{const} = \frac{V_{\text{Cu}_{6}\text{Sn}_{5}}}{6} \]

Calculations has proved that the value of \( \text{const} \) is approximately on the same order of magnitude as the experimental results. At the initial stage, the anode IMCs are thin compared with the width of joints, so the dissolution flux keeps relatively constant under equilibrium state. When the electric current density doubles, the flux of dissolution become twice (comparing the blue line and red line in Fig. 7d), and the cathode Cu substrate depletes much more seriously. Besides, according to previous research by M. L. Huang, the size of solder bump will influence the concentration distribution of Cu atoms in molten solder, and influence the growth rate of \( \text{Cu}_{6}\text{Sn}_{5} \). The model raised in our study also exhibits such size effect. By comparing the red line and yellow line in Fig. 7d, it can be seen that when the width \( L \) increases to \( L' \) under the same current density of \( 2j \), the Cu concentration difference at cathode increases from \( 2\Delta C \) to \( 4\Delta C \). So the dissolution flux and the growth rate of anode IMCs will increase accordingly. Therefore, this model can explain why the growth rate of \( \text{Cu}_{6}\text{Sn}_{5} \) observed by Haitao Ma is about 67 times larger than that observed in this study under an electric current density only 5 times higher. The main reason is that the joint in ref. 14 was about 400 \( \mu \text{m} \) in width, which was about 13 times larger than that in this study. So the Cu concentration at the cathode was much lower and could accelerate the dissolution. In addition, the increase of temperature will also increase the growth rate of \( \text{Cu}_{6}\text{Sn}_{5} \).

The formation of cellular morphology on the surface of \( \text{Cu}_{6}\text{Sn}_{5} \) grains under elevated electric current density and temperature could be explained by the theory of constitutional supercooling. The constitutional supercooling will result in the morphological instability of the solid-liquid interface and therefore lead to the formation of cellular microstructures. The requirement for forming cellular structures under constitutional supercooling can be expressed as:

\[ \frac{G}{R} < mC_s(1-k_0)/D_{\text{Cu}}^\text{liquid}k_0 \]

where \( R \) is the rate of deposition, \( G \) is the temperature gradient, \( k_0 \) is the solute distribution coefficient, and \( m \) is the slope of the liquidus. Based on Eq. 14, the increase of solute concentration \( (C_s) \) or deposition rate \( (R) \) can both increase the degree of constitutional supercooling. This kind of morphology change reflects the increase of both deposition rate and dissolution rate.

**Conclusions**

The morphology evolution and mechanical properties of \( \text{Cu}_{6}\text{Sn}_{5} \) intermetallic compounds under the applied current density of 1.0 \( \times \times 10^2 \) A/cm\(^2\) and 2.0 \( \times \times 10^2 \) A/cm\(^2\) at 260 \( ^\circ \text{C} \) and 300 \( ^\circ \text{C} \) in Cu/molten Sn/Cu interconnection system were investigated. The following conclusions were conducted:

1. The \( \text{Cu}_{6}\text{Sn}_{5} \) grew symmetrically in the joints reflowing without electric current, but showed obvious polarity effects reflowing under S-L EM. By contrast, the growth of Cu Sn was barely influenced by the electric current. Under elevated electric current density and temperature, cellular structures appeared on the surface of \( \text{Cu}_{6}\text{Sn}_{5} \) grains after long-time reaction.
2. The growth of \( \text{Cu}_{6}\text{Sn}_{5} \) reflowing at 260 \( ^\circ \text{C} \) followed a cubic root dependence on time, and the diffusion coefficient was calculated to be 9.98 \( \times \times 10^{-14} \) m\(^2\)/s. Under S-L EM, the cathode \( \text{Cu}_{6}\text{Sn}_{5} \) barely grew, while the anode \( \text{Cu}_{6}\text{Sn}_{5} \) grew following a linear relationship with time. The growth rate of anode \( \text{Cu}_{6}\text{Sn}_{5} \) was 0.107 \( \mu \text{m/min} \) under 1.0 \( \times \times 10^2 \) A/cm\(^2\) at 260 \( ^\circ \text{C} \) and was doubled to 0.212 \( \mu \text{m/min} \) when the electric current density increased to 2.0 \( \times \times 10^2 \) A/cm\(^2\). Besides, an elevated temperature of 300 \( ^\circ \text{C} \) could increase the growth rate of anode \( \text{Cu}_{6}\text{Sn}_{5} \) to 0.132 \( \mu \text{m/min} \) under 1 \( \times \times 10^2 \) A/cm\(^2\).
3. A growth kinetics model of \( \text{Cu}_{6}\text{Sn}_{5} \) based on Cu concentration gradient concerning size effect was...
established to explain the acceleration of anode Cu₆Sn₅ growth under electric current. This model proves that higher electric current density, higher temperature and larger joint width can enhance dissolution of cathode Cu, and accelerate the growth of anode Cu₆Sn₅. This model can be helpful to predict the growth rate of Cu₆Sn₅ in the joints of different sizes under different electric currents at soldering temperatures.

4. The Sn-based joints exhibited plastic fracture features within Sn phase and reached a shear strength of 42.69 MPa. The shear strength of Cu₆Sn₅-Sn mixed joints decreased dramatically because the mechanical property mismatching of Cu₆Sn₅ and Sn, and the fracture happened mainly along the Cu₆Sn₅-Cu₃Sn boundary. The Cu₆Sn₅-based joints exhibited brittle fracture and reached an average shear strength of 44.88 MPa. These results showed that full-Cu₆Sn₅ joints could achieve comparable shear strength with Sn-based joints as long as the defects and soft phase were removed.

Methods
Sample preparation. The samples used in this study were Cu/Sn/Cu sandwich structure. 1 mm-in-thickness, 99.99% purity Cu plates and 50 μm-in-thickness 99.95% purity Sn foils served as base metal substrates and interlayers, respectively. Both of them were cut into 2.5 × 2.5 mm² pieces. In order to minimize the contact resistance and voids/defects within the joints, the surface oxides and dirt were removed from the substrates and interlayers by slightly polishing for 1 min, and ultrasonic cleaning in acetone for 3 min. Flux was used in between to achieve better wettability.

Bonding process. The joints were bonded by an electric current-assisted bonding process using a specially-designed fixture, as shown in Supplementary Fig. S5. To ensure the thickness consistency among different samples and good contact between the sample and electrodes, an electrode pressure of 0.08 MPa was applied by two springs and calibrated by a dynamometer. The electric current was supplied by DC power. In Liu's study, the electric current density was as high as 10⁴ A/cm², completing the reaction in only 30 ms, which was not able to observe the reaction process. In order to slow the growth of Cu-Sn IMC, smaller electric current densities were chosen: 1.0 × 10² A/cm² and 2.0 × 10² A/cm² in this study. After assembly, the whole experimental setup was put into vacuum tube furnace to undergo solid-liquid electromigration at 260 °C and 300 °C with the times from 15 min to 960 min. The temperature at the joint was monitored in real time by thermocouple and maintained constant in the aid of a feedback system to eliminate the joule heating effect. Thus the effect of temperature and electric current density can be investigated separately.

Characterizations. After bonding, two groups of samples were prepared following the same procedure for cross-sectional characterization and shear tests, respectively. The first group of samples for cross-sectional observation were firstly mounted in acrylic resin and then carefully ground and polished. Afterwards, a Quanta 200FEG scanning electron microscope (SEM) with an energy dispersive X-ray spectroscopy microanalysis (EDS) was used to characterize the microstructure evolution and phase composition. The γ-Cu₆Sn₅ growing at the Sn side and the ε-Cu₆Sn₅ growing at the Cu side were of different brightness in SEM images, which can be abstracted by Photoshop software. The IMC thickness thus can be calculated. EPMA (EPMA-1600 Electron probe micro-analyzer) was used to measure the Cu concentration in Cu-Sn joints. Another group of samples were prepared to measure the shear strength using an XYZTEC Condor Sigma Bond Tester with a loading rate of 200 μm/s. The fractures were firstly observed using SEM, and then deeply etched by solution (10 vol. % HNO₃ + 90 vol. % H₂O) for 5 min to remove the residual Sn for revealing the 3D morphology of Cu₆Sn₅ grains.

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**Author Contributions**

Y.T. supervised the project; J.F. and B.L. performed the experiments; J.F., C.H. and C.W. discussed the results, and J.F. wrote the manuscript.

**Additional Information**

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