Abstract—We present a Virtual Kinematic Chain (VKC) perspective, a simple yet effective method, to improve task planning efficacy for mobile manipulation. By consolidating the kinematics of the mobile base, the arm, and the object being manipulated collectively as a whole, this novel VKC perspective naturally defines abstract actions and eliminates unnecessary predicates in describing intermediate poses. As a result, these advantages simplify the design of the planning domain and significantly reduce the search space and branching factors in solving planning problems. In experiments, we implement a task planner using Planning Domain Definition Language (PDDL) with VKC. Compared with conventional domain definition, our VKC-based domain definition is more efficient in both planning time and memory. In addition, abstract actions perform better in producing feasible motion plans and trajectories. We further scale up the VKC-based task planner in complex mobile manipulation tasks. Taken together, these results demonstrate that task planning using VKC for mobile manipulation is not only natural and effective but also introduces new capabilities.

I. INTRODUCTION

As one of the central themes in AI and robotics, task planning is typically solved by searching a feasible action sequence in a domain. Researchers have demonstrated a wide range of successful robotics applications [1, 2] with effective representations or programming languages, such as STRIPS [3], hierarchical task network [4], temporal and-or-graph [5, 6], Markov decision process [7], and PDDL [8].

An effective task planner in robotics generally possesses two characteristics. First, the planning domain must be clearly defined, which includes a set of predicates that truthfully describe the environment states, a set of actions that specify how states transit, and a goal specification that indicates the desired result. However, the definitions of these components are tightly coupled; thus, designing the planning domain could be tedious and error-prone. Second, the abstract notion of symbolic actions should be realizable by motion planners; i.e., the design of these abstract symbols should have practical meaning. These two requirements pose additional challenges in task planning for mobile manipulation; the robot consists of a mobile base and an arm, which possess different motion patterns and capabilities.

Efficient Task Planning for Mobile Manipulation:
a Virtual Kinematic Chain Perspective

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Fig. 1: A typical task planning setup, wherein the mobile manipulator is to tasked to navigate and pick up the object on the desk. The VKC-based domain specification reduces the search space by removing the poses of the mobile base near red cubes, resulting in a simpler and more intuitive task planning domain.

To clearly illustrate the above challenges, let us take Fig. 1 as a concrete example, wherein a mobile manipulator is tasked to navigate and pick up the bottle on the desk. A dedicated set of predicates and actions must be specified for the mobile base and the arm; for instance, moving the base (move(·)) to a configuration, such that the arm can pick up the object (pick(·)). Of note, finding such a pose oftentimes requires to specify the mobile base and the arm individually. However, this separation in the planning domain is artificial in nature and ineffectively introduces an unnecessarily larger planning space: The valid poses of the mobile base near the goal (i.e., the bottle) must be specified (indicated by the cubes in Fig. 1) in advance, and exactly one (e.g., the green cube) must be selected via sampling or searching under pre-defined heuristic or criteria. This deficiency becomes increasingly evident as the task sequence grows longer and prohibits natural motions that require foot-arm coordination; coordinating the base and arm movements remains challenging even for existing whole-body motion planning methods [9–11], let alone realizing a symbolic task plan with a feasible motion plan.

In this paper, we seek to tackle these challenges in task planning with a focus on domain specification. Specifically, we ask: (i) Is there an intermediate representation to facilitate the specification of the planning domain such that the search can be more natural and efficient, without relying on manually-designed heuristics? (ii) Can this new representation simplify the planning domain in long-horizon tasks while preserving motion feasibility, especially for those who require complex foot-arm coordination?
In particular, we propose a Virtual Kinematic Chain (VKC) perspective for mobile manipulation, which consolidates the kinematics of the mobile base, the arm, and the object being manipulated into a single kinematic model. By treating the robot as a whole, more abstract actions can be defined to jointly account for both the base and the arm; see pick-vkc(·) vs move(·) and pick(·) in Fig. 1. Such an abstraction alleviates the manually-defined heuristic of where the robot can reach the goal and the unnecessary definitions of intermediate goals, e.g., predicates describing the robot’s pose before reaching the goal. As a result, this modification of the planning domain reduces the branching factor, making it scalable to more complex tasks. Crucially, the abstraction introduced by VKC does not sacrifice the success rate to generate a solvable motion planning problem.

In experiments, we implement the VKC-based task planning using PDDL. Compared with a standard PDDL implementation, the VKC perspective simplifies the domain setup and exhibits significant improvements in planning time and memory. Moreover, we demonstrate that abstract actions introduced by VKC are executable at the motion level; they can generate solvable motion planning problems in the form of trajectory optimization or sampling methods. We further validate VKC-based task planning in long-horizon tasks requiring foot-arm coordination. Taking together, our VKC perspective offers a simple yet effective intermediate representation for domain specification in task planning.

A. Related Work

Task and Motion Planning (TAMP) in mobile manipulation: Thanks to the development of PDDL and other planning architectures, complex symbolic task planning can be solved using standard algorithms [2]. Hence, the community has shifted the focus to corresponding a valid symbolic action sequence to feasible motions, which leads to the field of TAMP [12]. While researchers tackle this problem from various angles, such as incorporating motion-level constraints to the task planning [13–15], developing interfaces that communicate between task and motion [16], or inducing abstracted modes from motions [17, 18], it remains a largely unsolved problem. In addition, movements of a mobile base and a manipulator are commanded by two or more separable actions [15, 19, 20], causing increased planning time, less coordinated movements, etc. In comparison, the VKC perspective serves as an intermediate representation that benefits the task modeling of mobile manipulation, improves computation efficacy, and facilitates motion planning.

VKC in robot modeling and planning: The idea of VKC could be traced back to 1997 by Pratt et al. [21], who proposed VKC to design bipedal robot locomotion [22]. Later, this idea was adopted to chain serial manipulators to form one kinematic chain [23] and to dual-arm manipulation tasks; for instance, connecting parallel structures via rigid-body objects [24], and modeling whole-body control of mobile manipulators [25]. Recently, VKC is also adopted for wheeled-legged robot control [26]. In this paper, we further push the idea of VKC and demonstrate its advantages as an intermediate representation in modeling and planning complex mobile manipulation tasks.

B. Overview

The remainder of this paper is organized as follows. Section II introduces the modeling process of constructing a VKC. A task planning framework from the VKC perspective based on PDDL is described in Section III. Section IV further illustrates how the high-level VKC-based task planning facilitates low-level motion planning. In a series of mobile manipulation tasks, we demonstrate the efficacy of VKCs with a high success rate in Section V. We conclude the paper with discussions in Section VI.

II. VIRTUAL KINEMATIC CHAIN (VKC) MODELING

The objective of the modeling is to construct a serial VKC \( C^V \) by composing the kinematic of the mobile base, the arm, and the object to be manipulated.

Original Structure: The kinematic models of the robot and the object being manipulated are represented by two kinematic trees, \( T^{GR} \) and \( T^{GO} \), respectively. The highlighted area in Fig. 2(c) indicates the original kinematic chain of interests: \( C^R \) for robots, and \( C^O \) for objects.

Kinematic Inversion: To construct a serial VKC by inserting a virtual joint (i.e., an attachment) between the robot’s end-effector frame \( F^{e}_E \) and the object’s attachable frame \( F^O \), one has to invert the kinematic relationship of the object \( C^O \) as shown in the right panel of Fig. 2(b). Note, such an inversion is not equivalent to simply reversing the parent-child relationship between the two adjacent links; the transformation between them must also be properly updated since a joint (i.e., revolute/prismatic) typically constrains the child link’s motion w.r.t. child link’s frame.

The spatial relationships between any two frames can be represented by a homogeneous transformation. A formal
inversion of kinematic chains with multiple links is given by:
\[ i-1T_{\text{inv}} = (i+1)^{T_{\text{inv}}} = \begin{bmatrix} i+1R^T & -i+1R^T & i+1^T \end{bmatrix} \]
where \( T \) is the transformation from the link \( a \) to the frame \( b \). Hence, \( i+1T \) is the transformation from the link \( v \) to the link \( i+1 \) in the original kinematic chain, whereas \( i-1T_{\text{inv}} \) represents the transformation from the link \( v \) to the link \( i-1 \) in the inverted kinematic chain. Eq. (1) describes the parent link of the link \( i \) in the original kinematic chain becomes the child link of the link \( i \) in the inverted kinematic chain, where the transformation of the inverted joint is given by \( i-1T_{\text{inv}} \).

**VKC Construction:** After inverting the object kinematic chain \( C^O \), a virtual kinematic chain can be constructed by adding a virtual joint (revolute, prismatic, or fixed) between \( F^O_{ui} \) and \( F^P_{ui} \), whose transformation is denoted as \( ^{\text{inv}}T \). Next, a virtual base, whose frame is \( F^B_{1} \), is further inserted to enable a joint optimization of the locomotion and manipulation. Two perpendicular prismatic joints and a revolute joint are added between the virtual base and the robot base to imitate a planar motion between the mobile base and the ground, while ensuring the virtual kinematic chain \( CV^V \), highlighted by red in Fig. 2b, remains serial.

Fig. 2d shows a constructed VKC in opening a door. The above procedure produces a serial kinematic chain: Its base is a virtual fixed link in the environment, and its end-effector is at the link of the door that connects to the ground. The mobile base and the arm become the links embedded in the chain, and their poses during the door opening are calculated implicitly given the end-effector pose (i.e., the angle of the revolute hinge of the door). In other words, the final robot state is jointly optimized with trajectory, task goal, and kinematic constraints, without further efforts on finding the robot goal state or goal space for trajectory generation. This example demonstrates the possibilities to design robot actions and predicates without explicitly specifying the complete robot goal state (see Section III) while still being plausible at the motion level (see Section IV).

### III. TASK PLANNING ON VKC

Following the classic formalization of task planning, we describe the environment by a set of states \( S \). Possible transitions between these states are defined by \( \mathcal{T} \subseteq S \times S \), where a transition \( t = (s,s') \in \mathcal{T} \) alters the environment state from \( s \in S \) to \( s' \in S \). The goal of the task planning problem is to identify a sequence of transitions that alters the environment from its initial state \( s_0 \in S \) to a goal state \( s_g \in S_g \), where \( S_g \subseteq S \) is a set of goal states.

We primarily consider the task planning problems in mobile manipulation, which require the robot to account for its base, arm, and the object being interacted (e.g., pick and place, door/drawer opening). We formulate the task planning problems and implement the planning domains using PDDL.

In PDDL, the environment state \( s \) is described by a set of predicates that hold true. Specifically:

- \( \text{vkcState} \ ?r \ ?q \): A sub-chain \( ?r \) (e.g., the base, an arm, or even a VKC) of a VKC is at configuration \( ?q \) in joint space.
- \( \text{objConf} \ ?o \ ?s \): An object \( ?o \) is at the configuration \( ?s \) in SE(3).
- \( \text{free} \ ?v \): The robot end-effector is free to grasp.
- \( \text{carry} \ ?o \ ?v \): The robot end-effector is carrying an object \( ?o \).

In this paper, to focus on demonstrating the benefit of task planning with VKC, we pre-sampled feasible configurations \( ?s \) for all objects and corresponding grasping poses.

Transitions in PDDL are modeled by actions. Each action takes parameters as input and can be called only when its preconditions hold true. After an action is called, its effect indicates how the states in the current environment change from preconditions. Thanks to the advantages introduced by the VKC, three simple action definitions—\( \text{goto-vkc}, \text{pick-vkc}, \text{and-place} \)—are sufficient to handle various mobile manipulation tasks, from pick-and-place in different setups to foot-arm coordinated and constrained motions (e.g., door/drawer opening). Below is an example of the definitions for three actions; see Figs. 4b and 4c and Section V-A for a comparison between VKC-based PDDL and a standard PDDL for mobile manipulators.

```lisp
:(action goto-vkc
  :parameters (?r ?from ?to)
  :precondition (vkcState ?r ?from)
  :effect (and (vkcState ?r ?to)
               (not (vkcState ?r ?from)))
)

:(action pick-vkc
  :parameters (?o - obj ?s - state ?v - vkc)
  :precondition (and (objConf ?o ?s) (free ?v))
  :effect (and (carry ?o ?v)
               (not (objConf ?o ?s))
               (not (free ?v)))
)

:(action place-vkc
  :parameters (?o - obj ?s - state ?v - vkc)
  :precondition (and (carry ?o ?v)
                     (not (occupied ?s)))
  :effect (and (not (carry ?o ?v))
             (objConf ?o ?s)
             (free ?v)))
```

### IV. VKC FACILITATES MOTION PLANNING

The conventional task planning setup usually assumes a robot already knows how to execute the actions defined in the task domain and, therefore, does not generate actionable motion trajectories for the robot. However, in practice, this assumption does not always hold as many abstract actions defined in the task domain are difficult to be instantiated at the motion level. This section discusses how the actions defined using VKC can properly form a motion planning problem solvable by existing motion planners.

A. From Task to Motion

We start by making the connections between the action semantics and the actual manipulation behaviors, followed by explaining how the predicates and variables in the action definitions are processed by motion planners.
B. Optimization-based Motion Planning

Tasks can be formulated by trajectory optimization, e.g., CHOMP [27] and TrajOpt [28]. The objective function of tasks that mobile manipulators stop interacting with the environment or itself. The problem of motion planning on various task-specific requirements. In this paper, we further impose several additional safety constraints, including joint limits, bounds for joint velocity and acceleration, and link- and link-object collisions. A more detailed analysis of the optimization framework can be found in Jiao et al. [29].

C. Sampling-based Motion Planning

Alternatively, motion planning on VNC can also be viewed as a search procedure in the configuration space $Q_{free}$. Given a path planning problem within $Q_{free}$, a sampling-based method would attempt to find a set of collision-free way points that start from an initial configuration $q_0 \in Q_{free}$ and end in the goal configuration $q_{goal} \in Q_{free}$.

Rapidly-exploring Random Tree (RRT) is a probabilistically complete search algorithm that incrementally expands a collection of directional nodes $T$ to explore space [30]. In this paper, we adopted a RRT-connect algorithm [31] from the Open Motion Planning Library (OMPL) [32] as our sampling-based motion planner, which initiates exploration from $q_0$ and $q_{goal}$ concurrently.

Unlike the optimization-based method mentioned in Section IV-B, way-points collected by RRT-connect are not smoothed by an objective function during search; instead, interpolation was performed after the search is complete for a smooth trajectory to be executed on a mobile manipulator.
V. Experiment

We conduct a series of experiments to evaluate the efficacy of the proposed VKC perspective for planning mobile manipulation tasks in simulations. The first experiment compares the designs of PDDL definition with VKC or without VKC and their corresponding planning efficiency. Since the action definitions can be arbitrarily abstract at the symbolic task level, we further validate the VKC-based action design in the second experiment that it indeed provides sufficient information for motion planners to produce feasible trajectories. Finally, in the third experiment, we showcase how the VKC perspective empowers more complex task planning.

A. Simplifying Task Domain

Since the VKC perspective treats the base, the arm, and the object to be manipulated as a whole, designing the planning domain becomes much simpler. In this experiment, we focus on an object-arrangement task, where the robot is tasked to re-arrange \( m \) objects on \( m + 1 \) tables into the desired order while satisfying the constraint that each table can only support one object. Fig. 4a shows a typical example of this task’s initial and goal configuration with \( m = 8 \) objects, randomly sampled in each experimental trial.

Fig. 4b shows a PDDL domain designed by the actions mentioned in Section III, which requires less predicates and provides more abstract actions compared with those designed by conventional domain definition shown in Fig. 4c. Specifically, the conventional method would require (i) more predicates to describe the mobile base’s states and thus more complex preconditions for actions, (ii) one more action to control the mobile base, and (iii) more parameters for other actions. To solve for a task plan, we adopt the Iterated Width Search (IWS) algorithm [33]; it is a width-limited version of the Breadth First Search (BFS) that repeatedly runs with increasing width limits until a feasible task plan is found. If no feasible task plan could be found within the maximum width limit of the IWS, a traditional BFS with no width limit will be deployed to search for a solution.

In experiments, we run 50 trials for each setup; see the result summary in Fig. 4d. As the task complexity increases, the average planning time and the number of nodes generated in search (i.e., memory required) increase relatively slowly for the VKC-based task plan. In comparison, the baseline using conventional methods increases much more rapidly.

This result is evident. As we can see in Fig. 4d, planning in the non-VKC version of the task domain requires exploring more nodes at each depth level to find a plausible pose for the mobile base. It also requires more actions to accomplish the task, which further yields a deeper depth during the search. Suppose there are \( N \) nodes on average to be generated at each depth level of the search algorithm, and a feasible solution is found at depth \( d \), the total number of nodes being generated is \( N^d \). In theory, when the search algorithm performs in the VKC domain, the total number of generated node is \( (c_1N)^{c_2d} \), where \( c_1 \leq 1, c_2 \leq 1 \). In the task with 16 objects, our experiment empirically finds \( c_1 = 0.75 \) and \( c_2 = 0.22 \) on average over 50 trails.

Taken together, the results in the first experiment demonstrated that VKC-based task planning requires much fewer

B. Improving Mobile Manipulation

In general, actions that are more abstract and with fewer variables in the planning domain specification would lead to more efficient task planning, but simultaneously could result in less success rate in generating feasible plans at the motion level. In this experiment, we validate that the VKC-based task planning provides efficacy at the task level and maintains a high success rate at the motion level. Based on the generated task plans (i.e., action sequences) and the encoded information (as described in Section IV), we apply a trajectory optimization-based motion planner and a sampling-based motion planner and evaluate how well they can produce feasible motion trajectories for the given task.

Specifically, we consider the task of pulling opening a drawer; see Fig. 5a. The task plans: (i) place--vkc (drawer, \( s_1 \), vkc), (ii) move (\( q_0, q_1 \)) place (drawer, \( s_1 \), arm, \( q_0 \)), are produced by two PDDLs specified with and without VKC, respectively. We compare the success rate of executing the trajectories planned by trajectory optimization and sampling motion planning methods described in Sections IV-B and IV-C as well as the base and arm cost.
measured by the distances they travel; see Fig. 5b.

The trajectory optimization-based motion planner can produce feasible trajectories for the given task with high success rates; the produced trajectories are more efficient in terms of shorter base and arm traveling distances. Typically, sampling-based motion planners would struggle in incorporating kinematic and safety constraints due to naturally unconstrained configuration spaces, which need extra effort to accommodate extra kinematic constraints [34], making it less suitable for such tasks. However, it is still more successful in producing feasible trajectories under the VKC specification compared with the setting without VKC. The most significant drawbacks of sampling-based motion planners are the high execution costs and violation of safety limits.

C. Solving Tasks with Multiple Steps

Complex multi-step mobile manipulation tasks with long action sequences can also be easily accomplished using the action set introduced by the VKC-based task planner described in Section III. These actions contain high-level task semantics that could be adapted to various tasks; e.g., attaching to the doorknob could be expressed by a pick-vkc action, and open the door to a certain angle could be expressed by a place-vkc.

Fig. 6a qualitatively shows a complex multi-step task planning using the VKC-based domain specification and instantiating that to motions. For a more fair comparison, in addition to the initial and goal state of the environment, both the VKC and non-VKC methods are provided with the (identical) grasping poses for all movable objects, but not the corresponding robot state. In this task, a mobile manipulator needs to (i) grasp the stick, (ii) fetch the cube under the table using the stick, which is otherwise challenging to reach, (iii) move the cube outside, (iv) place the stick down, (v) grasp the cabinet and open it, (vi) place the cube inside the cabinet, and (vii) close the cabinet door. At each trial, the mobile manipulator is randomly placed in the environment.

Fig. 6b illustrates that the above complex multi-step task can be accomplished by using only two abstract actions defined based on VKC, one action in each step. Without the VKC perspective, significantly more effects must be precisely analyzed, and each step may require several actions to be executed together; see Table I for a comparison between the two setups. Even after the additional efforts of specifying base pose from a feasible region, its accumulated success rate at the motion level produced by the corresponding actions still underperforms the VKC version, shown in Fig. 6c.

Without VKC, the motion planner particularly suffers at step 2 when the robot needs to fetch the cube in a confined space, as it requires the planner to deliver proper navigation and manipulation with excellent foot-arm coordination (i.e., coordinating move and place). In sum, this experiment demonstrates that VKC-based mobile task planning for mobile manipulation tasks is advantageous by simplifying domain specification and improving motion planning.

TABLE I: Actions and predicates in the defined planning domains. Without VKC, more actions must be specified, and extra predicates are required for generating a feasible task plan.

| Setup | Group | Notation | Description |
|-------|-------|----------|-------------|
| Actions | pick-vkc(o,v) | see Section III |
| Predicates | } | |
| | Geometric(o,v) | Check if robot r is able to grasp object o |
| | Rigid(o) | Check if object o is rigid object |
| | Articulated(o) | Check if object o is articulated object |
| | Tool(o) | Check if object o could be used as a tool |
| | Occupied(q) | Check if a position q is occupied |
| | Carried(r) | Check if an object o is carried by robot r |
| | ContainerSpace(o) | Check if a position q is contained in the object o |
| Extra | MoveObject(x) | More robot from x1 to x2 |
| | PickObject(o) | Pick the object o at location x2 given robot state s2 |
| | PlaceObject(o) | Place the object o at location x2 given robot state s2 |
| | OpenObject(o) | Open the object at location x3 given robot state s3 |
| | CloseObject(o) | Close the object at location x3 given robot state s3 |
| |Reachable(s) | Check if robot at state s is able to do pick action |
| | AbleToPick(o) | Check if object o is reachable by mobile base at state s |

VI. DISCUSSION AND CONCLUSION

We present a VKC perspective that improves the domain specifications for mobile manipulation task planning. By integrating the kinematics of the mobile base, the arm, and the object to be manipulated into a single VKC, more abstract action symbols become possible and fewer predicates/variables/intermediate goals are required in designing the planning domain. In a series of experiments, we demonstrate that the VKC-based domain specification using PDDL supports more efficient task planning, works better with existing motion planners, and scales up to more complex tasks compared with the one without VKC. We argue the proposed VKC perspective has significant potential in promoting mobile manipulation in real-world daily tasks. Our future work will explore TAMP on VKC.

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possessing an excellent foot-arm coordination in each step of the task. Without VKC, to ensure successful planning for tasks that require foot-arm coordination, several actions must be executed together to complete certain steps in the task.

Fig. 6: (a) The VKC-based task planner can easily scale up to a complex multi-step task, which can be (b) succinctly expressed by merely two actions defined based on the VKCs. (c) More abstract action definitions introduced by VKC instantiate better at the motion level.

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