THE ORIGIN OF THE MASS-METALLICITY RELATION: INSIGHTS FROM 53,000
STAR-FORMING GALAXIES IN THE SLOAN DIGITAL SKY SURVEY

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ABSTRACT

We utilize Sloan Digital Sky Survey imaging and spectroscopy of ∼53,000 star-forming galaxies at z ∼ 0.1 to study the relation between stellar mass and gas-phase metallicity. We derive gas-phase oxygen abundances and stellar masses using new techniques that make use of the latest stellar evolutionary synthesis and photoionization models. We find a tight (±0.1 dex) correlation between stellar mass and metallicity spanning over 3 orders of magnitude in stellar mass and a factor of 10 in metallicity. The relation is relatively steep from 10^8.5 to 10^{10.5} M_☉, h^7_{⊙}, in good accord with known trends between luminosity and metallicity, but flattens above 10^{10.5} M_☉. We use indirect estimates of the gas mass based on the Hα luminosity to compare our data to predictions from simple closed box chemical evolution models. We show that metal loss is strongly anticorrelated with baryonic mass, with low-mass dwarf galaxies being 5 times more metal depleted than L* galaxies at z ∼ 0.1. Evidence for metal depletion is not confined to dwarf galaxies but is found in galaxies with masses as high as 10^{10} M_☉. We interpret this as strong evidence of both the ubiquity of galactic winds and their effectiveness in removing metals from galaxy potential wells.

Subject headings: galaxies: abundances — galaxies: evolution — galaxies: fundamental parameters — galaxies: statistics

1. INTRODUCTION

Stellar mass and metallicity are two of the most fundamental physical properties of galaxies. Both are metrics of the galaxy evolution process, the former reflecting the amount of gas locked up into stars, and the latter reflecting the gas reprocessed by stars and any exchange of gas between the galaxy and its environment. Understanding how these quantities evolve with time and in relation to one another is central to understanding the physical processes that govern the efficiency and timing of star formation in galaxies.

The influence of stellar winds and supernovae on the interstellar medium (ISM) of galaxies, generally dubbed “feedback,” has been regarded as an important ingredient in galaxy evolution since the 1970s (Larson 1974; Larson & Dinerstein 1975; White & Rees 1978). Feedback is believed to play a critical role in regulating star formation by reheating the cold ISM and by physically removing gas from the disk and possibly the halo via galactic winds. Various lines of observational evidence have established that large-scale outflows of gas are ubiquitous among the most actively star-forming galaxies at low and high redshift (e.g., Lehnert & Heckman 1996; Dahlem et al. 1998; Rupke et al. 2002; Shapley et al. 2001; Frye et al. 2002). However, detailed studies of winds in nearby starbursts have shown them to be a complex, multiphase, hydrodynamical phenomenon with the majority of the energy and newly synthesized metals existing in the hard-to-observe coronal and hot phases (T = 10^5–10^7 K; e.g., Strickland et al. 2002). This complexity has prevented both a direct assessment of the cosmological impact of galactic winds and the development of physically accurate prescriptions for incorporating feedback into semianalytical and numerical models of galaxy formation.

Fortunately, it is possible to obtain some quantitative information about the impact of galactic winds without a full understanding of the abstruse physics responsible for their morphology and kinematics. Galaxies that host winds powerful enough to overcome the gravitational binding energy of their halos will vent some of their metals into the intergalactic medium. Hence, one way of evaluating the importance of galactic winds is to look for their chemical imprint on galaxies. However, low metallicity is not necessarily a hallmark of wind activity. The metallicity of a galaxy is expected to depend strongly on its evolutionary state, namely, how much of its gas has been turned into stars. To detect metal depletion, it is therefore necessary to make some assumptions about the expected level of chemical enrichment based on a galaxy’s star and gas content. Of course, other mechanisms besides winds could make a galaxy appear to be metal depleted, for example, the inflow of pristine gas, or the return of comparatively unenriched material from evolved low-mass stars. However, these...
scenarios can potentially be distinguished by examining the dependence of metal depletion on dynamical mass. To quantify the impact of feedback on the local galaxy population, we therefore compare the observed metallicities of galaxies spanning a wide range in total mass to the predictions of simple chemical evolution models.

Interest in the relationship between mass and metallicity dates back several decades, beginning with the seminal work of Lequeux et al. (1979). However, because of the difficulty of obtaining masses, luminosity was generally adopted as a surrogate. A correlation between metallicity and blue luminosity was demonstrated by Garnett & Shields (1987) and extended by various authors (e.g., Skillman et al. 1989; Brodie & Huchra 1991; Zaritsky et al. 1994) to include a range of Hubble types and to span over 11 magnitudes in luminosity and 2 dex in metallicity. The interpretation of this striking trend has, however, remained a matter of some debate owing to the difficulty of transforming from observables to the ingredients needed for simple chemical evolution models (stellar mass, gas mass, and metallicity).

In recent years, the development of more sophisticated models for stellar populations (e.g., Bruzual & Charlot 2003, hereafter BC03) and gaseous nebulae (e.g., Ferland 1996; Charlot & Longhetti 2001) has resulted in major advances in our ability to derive physical properties from observables. In this work we derive stellar mass-to-light (M/L) ratios according to the methods of Kauffmann et al. (2003a), which rely on spectroscopic line indices to help circumvent the classical age-metallicity-reddening degeneracy issues. We measure metallicity using the formalism of S. Charlot et al. (2004, in preparation), which makes use of all of the strong optical nebular lines in our bandpass (as opposed to more traditional methods that rely on a single line ratio). We couple these improved techniques with the enormous statistical power provided by the Sloan Digital Sky Survey (SDSS). We present the mass-metallicity relation of \( \sim 53,000 \) star-forming galaxies at \( z \sim 0.1 \) as a new benchmark for successful models of galaxy evolution.

We begin with a brief description of the SDSS data products and our data processing techniques in § 2. We outline our method for measuring metallicity and stellar mass in § 3. In § 4 we compare the luminosity-metallicity relation of the SDSS data with previous determinations. We present the mass-metallicity relationship in § 5 and consider its origin in § 6. We explore sources of systematic error in § 7 and conclude in § 8.

Where appropriate we adopt a cosmology of \( \Omega_M = 0.3 \), \( \Omega_\Lambda = 0.7 \), and \( H_0 = 70 \text{ km} \text{ s}^{-1} \text{ Mpc}^{-1} \).

2. THE SDSS DATA

The data analyzed in this study are drawn from the SDSS. The survey goals are to obtain photometry of one-quarter of the sky and spectra of nearly one million objects. Imaging is obtained in the \( u, g, r, i, z \) bands (Fukugita et al. 1996; Smith et al. 2002) with a special-purpose drift scan camera (Gunn et al. 1998) mounted on the SDSS 2.5 m telescope at Apache Point Observatory. The imaging data are photometrically (Hogg et al. 2001) and astrometrically (Pier et al. 2003) calibrated and used to select stars, galaxies, and quasars for follow-up fiber spectroscopy. Spectroscopic fibers are assigned to objects on the sky using an efficient tiling algorithm designed to optimize completeness (Blanton et al. 2003a). The details of the survey strategy can be found in York et al. (2000), and an overview of the data pipelines and products is provided in the Early Data Release paper (Stoughton et al. 2002).

Our parent sample for this study is composed of 211,265 objects that have been spectroscopically confirmed as galaxies and have data publicly available in the SDSS Data Release 2 (DR2; Abazajian et al. 2004). These galaxies are part of the SDSS “main” galaxy sample used for large-scale structure studies (Strauss et al. 2002) and have Petrosian \( r \) magnitudes in the range \( 14.5 < r < 17.77 \) after correction for foreground galactic extinction using the reddening maps of Schlegel et al. (1998). Their redshift distribution extends from \( \sim 0.005 \) to 0.3, with a median \( z \) of 0.10. From this sample we select a subset of 53,400 star-forming galaxies for nebular analysis, as discussed in § 2.2.

We determine stellar mass-to-light ratios and nebular metallicities for our sample galaxies from the SDSS spectra. The spectra are obtained with two 320-fiber spectrographs mounted on the SDSS 2.5 m telescope. Fibers \( 3'' \) in diameter are manually plugged into custom-drilled aluminum plates mounted at the focal plane of the telescope. The spectra are exposed for 45 minutes or until a fiducial signal-to-noise ratio (S/N) is reached. The median S/N per pixel for galaxies in the main sample is \( \sim 14 \). The spectra are processed by an automated pipeline (D. J. Schlegel et al. 2004, in preparation) that flux and wavelength calibrates the data from 3800 to 9200 Å. The instrumental resolution is \( R = \lambda / \delta \lambda = 1850 - 2200 \) (FWHM \( \sim 2.4 \) Å at 5000 Å).

The wavelength coverage, resolution, S/N, and general high quality of the SDSS spectra make them extremely well suited for the derivation of nebular abundances. However, the spectrophotometric calibration and the small size of the fiber aperture relative to the target galaxies pose some concern. The SDSS spectrographs do not employ an atmospheric dispersion corrector, and the spectra are frequently acquired under non-photometric conditions. The survey has nevertheless been able to obtain a remarkable level of spectrophotometric precision by the simple practice of observing multiple standard stars simultaneously with the science targets. (The artifact in this case is that the “standards” are not classical spectrophotometric standards but are halo F subdwarfs that are calibrated to stellar models; see Abazajian et al. 2004 for details.) To quantify the quality of the spectrophotometry, we have compared magnitudes synthesized from the spectra with SDSS photometry obtained with an aperture matched to the fiber size. The \( 1 \sigma \) error in the synthetic colors is 5% in \( g - r \) and 3% in \( r - i \) \( (\Delta g \sim 4700 \AA; \Delta r \sim 6200 \AA; \Delta i \sim 7500 \AA) \). At the bluest wavelengths \( (\sim 3800 \AA) \) we estimate the error to be \( \sim 12\% \) based on repeat observations. There is also a systematic error in the sense that the spectra are bluer than the imaging by \( \sim 2\% \) in the \( g \) band, but it is unclear at present whether this represents an error in the absolute calibration of the photometry or the spectroscopy. While the random errors in the spectrophotometry are offset by the large size of the data set, the accuracy of our measured nebular abundances relative to true global abundances is compromised to some degree by the size of the fiber aperture. At the median redshift of the SDSS main galaxy sample (\( z \sim 0.1 \)) the target galaxies subtend several arcseconds on the sky. The fraction of galaxy light falling in the \( 3'' \) fiber aperture is typically about \( \frac{1}{2} \), with variations in redshift and morphological type causing the fraction to range from 0.05 to 0.6. The impact of this “aperture bias” is discussed in § 7.

2.1. Emission-Line Measurement

The emphasis of this study is on the nebular emission line spectra of galaxies. However, we cannot disregard the fact
that the optical spectra of galaxies are very rich in stellar absorption features, which can complicate the measurement of nebular emission lines. In order to maintain speed and flexibility, the SDSS spectroscopic pipeline performs a very simple estimate of the stellar continuum using a sliding median. While this is generally adequate for strong emission lines, a more sophisticated treatment of the continuum is required to recover weak features and to properly account for the stellar Balmer absorption, which can reach equivalent widths of 5 Å in some galaxies. To address this need, we have designed a special-purpose code optimized for use with SDSS galaxy spectra that fits a stellar population model to the continuum. We adopt the basic assumption that any galaxy star formation history can be approximated as a sum of discrete bursts. Our library of template spectra is composed of single stellar population models generated using the new population synthesis code of BC03. The BC03 models incorporate an empirical spectral library (Le Borgne et al. 2003) with a wavelength coverage (3200–9300 Å) and spectral resolution (~3 Å) that is well matched to that of the SDSS data. Our templates include models of 10 different ages (0.005, 0.025, 0.1, 0.2, 0.6, 0.9, 1.4, 2.5, 5, 10 Gyr) and three metallicities (0.1, 1, and 2.5 Z⊙). For each galaxy we transform the templates to the appropriate redshift and velocity dispersion and resample them to match the data. To construct the best-fitting model, we perform a nonnegative least-squares fit with dust attenuation modeled as an additional free parameter. In practice, our ability to simultaneously recover ages and metallicities is strongly limited by the S/N of the data. Hence, we model galaxies as single-metallicity populations and select the metallicity that yields the minimum χ². (While this is not particularly physical, in practice it is not a bad assumption since the integrated light of a galaxy tends to be dominated by the light of its most recent stellar generation.) The details of the template fitting code will be presented in C. A. Tremonti et al. (2004, in preparation). Figure 1 shows some typical spectra and their continuum models.

After subtracting the best-fitting stellar population model of the continuum, we remove any remaining residuals (usually of order a few percent) with a sliding 200 pixel median and fit the nebular emission lines. Since we are interested in recovering very weak nebular features, we adopt a special strategy: we fit all the emission lines with Gaussians simultaneously, requiring that all of the Balmer lines (Hα, Hγ, Hβ, and Hα) have the same line width and velocity offset, and likewise for the forbidden lines ([O ii] λλ3726, 3729, [O iii] λλ4959, 5007,
[N ii] λ6548, 6584, [S ii] λ6717, 6731). We are careful to take into account the wavelength-dependent instrumental resolution of each fiber, which is measured for each set of observations by the SDSS spectroscopic pipeline from the arc lamp images. The virtue of constraining the line widths and velocity offsets is that it minimizes the number of free parameters and effectively allows the stronger lines to be used to help constrain the weaker ones. Extensive by-eye inspection suggests that our continuum and line fitting methods work well.

2.2. The Galaxy Sample

From our original sample of ~211,000 galaxies, we select a subsample of star-forming galaxies for nebular analysis. We start by imposing a redshift cut of 0.005 < z < 0.25 and requiring that greater than 10% of the total galaxy light be observed by the fiber. Because stellar mass and metallicity are derived using Bayesian techniques (see § 3), it would be possible to select a sample of objects with accurate masses and metallicities using the likelihood distributions. However, for clarity we have opted to define our sample based on observables (line fluxes, line indices) and later make some weak cuts based on the derived parameters. We require galaxies included in our star-forming sample to have lines of Hβ, Hα, and [N ii] λ6584 detected at greater than 5σ. We do not explicitly constrain the other nebular lines that we make use of ([O iii] λλ3726, 3792, [O ii] λ5007, [S ii] λλ6717, 6731) because our Bayesian analysis takes into account the errors in the line fluxes. We note that [O ii] is not measured at z < 0.03 owing to the blue wavelength cutoff of the spectrographs. This affects 5% of our sample but has a negligible impact on our nebular analysis because we use multiple lines (see § 3.1). We impose the requirement that the parameters needed for mass determination have small errors (see § 3.2). These criteria are $\sigma(m_{\text{star}}) < 0.15$ mag, $\sigma(H_\alpha) < 2.5$ Å, and $\sigma(D_n(4000)) < 0.1$. The combination of these constraints trims the sample to ~82,000 galaxies, with the limiting factor typically being the strength of the Hβ line.

We remove galaxies harboring an active galactic nucleus (AGN) from our sample using the traditional line diagnostic diagram [N ii]/Hα versus [O iii]/Hβ (Baldwin et al. 1981; Veilleux & Osterbrock 1987). The division between star-forming galaxies and AGNs has been calibrated theoretically (Veilleux & Osterbrock 1987). The boundary between early and late types. As expected, our emission-line sample has bluer colors and more late-type morphologies than the parent sample. The redshift distribution is similar to that of the main survey and peaks around z = 0.08.

3. THE PHYSICAL PROPERTIES OF GALAXIES

3.1. Measuring Metallicity

We derive oxygen abundances for our SDSS galaxies from the optical nebular emission lines. There are a number of advantages of measuring metallicity from the nebular lines rather than the stellar absorption features via Lick indices (Worthey 1994). First, the S/N in the emission lines can greatly exceed that in the continuum, with the added advantage that many of the optically faintest galaxies (dwarfs) exhibit the highest emission-line equivalent widths. Second, nebular abundance determination is free of the uncertainties due to age and α-element enhancement that plague the interpretation of absorption-line indices. Third, nebular metallicities are easier to interpret in the context of chemical evolution models because they reflect the present-day metal abundance rather than the luminosity-weighted average of previous stellar generations. The disadvantage is that our sample is limited to galaxies with ongoing star formation.

The word “metallicity” has been used variously in the literature. In stellar studies metallicity usually refers to the iron abundance. Oxygen has been adopted as the canonical “metal” for ISM studies because it is the most abundant, it is only weakly depleted onto dust grains, and it displays strong lines in the optical. Hereafter we use metallicity to denote the gas-phase oxygen abundance measured in units of 12 + log(O/H), where the ratio O/H is the abundance by number of oxygen relative to hydrogen. Solar metallicity in these units is 8.69 (Allende Prieto et al. 2001) and LMC and SMC metallicities are 8.4 and 8.0, respectively (Garnett 1999).
The strong optical nebular lines of elements other than H and He are produced by collisionally excited transitions. The strength of these lines is the product not only of the heavy-element abundance but also the temperature, density, and ionization state of the nebula, the attenuation by dust, and the depletion of metals onto dust grains. In practice, direct determination of element abundances from optical emission lines tends to be limited by the faintness of the [O III] λ4363 line, which is used to determine the electron temperature. When the electron temperature cannot be measured directly, oxygen abundances can be estimated using empirically or theoretically calibrated relations between metallicity and the relative fluxes of various strong optical emission lines. “Strong-line” abundance calibration was pioneered by Alloin et al. (1979) and Pagel et al. (1979). The latter introduced the $R_{23}$ metallicity indicator $R_{23} = ([\text{O} \text{ III}] \lambda 5007 + [\text{O} \text{ II}] \lambda 3727 + [\text{O} \text{ II}] \lambda 4959, 5007)/\text{H} \beta$, which has enjoyed widespread use. Various other line ratios have been calibrated as metallicity indicators, including $[\text{N} \text{ II}] \lambda 6584/\text{H} \alpha$, $[\text{O} \text{ III}] \lambda 5007/[\text{N} \text{ II}] \lambda 6584$, $[\text{N} \text{ II}] \lambda 6584/[\text{O} \text{ II}] \lambda 3727$, and $([\text{S} \text{ II}] \lambda \lambda 6717, 6731 + [\text{S} \text{ III}] \lambda 9069, 9532)/\text{H} \beta$. Systematic differences among the various strong-line calibrations can exceed 0.2 dex (see Kewley & Dopita 2002 for a review).

Here we measure metallicities in a slightly more refined way, using the approach outlined by S. Charlot et al. (2004, in preparation). This consists of estimating metallicity statistically, based on simultaneous fits of all the most prominent emission lines ($[\text{O} \text{ II}]$, Hβ, $[\text{O} \text{ III}]$, Hα, $[\text{N} \text{ II}]$, $[\text{S} \text{ II}]$) with a model designed for the interpretation of integrated galaxy spectra (Charlot & Longhetti 2001). The Charlot & Longhetti (2001) model is based on a combination of the Bruzual & Charlot (1993) and Ferland (1996, ver. C90.04) population synthesis and photoionization codes. In this model, the contributions to the nebular emission by H ii regions and diffuse ionized gas are combined and described in terms of an effective (i.e., galaxy averaged) metallicity, ionization parameter, dust attenuation at 5500 Å, and dust-to-metal ratio. The depletion of heavy elements onto dust grains and the absorption of ionizing photons by dust are included in a self-consistent way. Charlot & Longhetti (2001) calibrated the emission-line properties of their model using the observed $[\text{O} \text{ III}]/\text{H} \beta$, $[\text{O} \text{ II}]/[\text{O} \text{ III}]$, $[\text{S} \text{ II}]/\text{H} \alpha$, and $[\text{N} \text{ II}]/[\text{S} \text{ II}]$ ratios of a representative sample of 92 nearby spiral, irregular, starburst, and H ii galaxies. The model also accounts well for the properties of these lines in our sample (Brinchmann et al. 2004, Fig. 5). We calculate the likelihood distribution of the metallicity of each galaxy in our sample, based on comparisons with a large library of models ($\sim 2 \times 10^5$) corresponding to different assumptions about the effective gas parameters. We adopt the median of this distribution as our best estimate of the galaxy metallicity; the width of the likelihood distribution provides a measure of the error. The median 1 σ error for our sample of star-forming galaxies is 0.03 dex. We note that this does not include systematic error. Because our metallicities are discretely sampled, we have added small random offsets for display purposes. These have a Gaussian distribution with $\sigma = 0.02$ dex.

Our models implicitly assume that the nebular gas in a galaxy can be characterized by a set of galaxy-averaged physical properties. An important issue is whether truly representative abundances can be derived for spatially integrated galaxy spectra in the presence of radial variations in temperature, ionization, metallicity, and dust extinction (Vila-Costas & Edmunds 1992; Zaritsky et al. 1994; Martin & Roy 1994; van Zee et al. 1998). Kobulnicky et al. (1999) addressed this issue by comparing H ii region abundances at particular disk radii with abundances measured from integrated spectra. They found excellent agreement ($\pm 0.05$ dex) when metallicities were based on $R_{23}$. However, the study is limited in one respect: they use weighted averages of the H ii region spectra as proxies for true integrated spectra, thereby ignoring the contribution of the diffuse ionized gas, which can be responsible for 25%–70% of the Balmer line emission (Martin 1997; Zurita et al. 2000; Thilker et al. 2002). Hence, further study is needed to quantify the systematics associated with true integrated abundances.

To place our metallicity measurements in the context of previous work, we show the relation between our derived metallicities and the line ratio $R_{23} = ([\text{O} \text{ II}] + [\text{O} \text{ III}])/\text{H} \beta$ in Figure 3. For comparison we show the theoretical relation between $R_{23}$ and metallicity derived by McGaugh (1991), the empirical relation defined by Edmunds & Pagel (1984), and the semiemipirical relation of Zaritsky et al. (1994), itself an average of three previous calibrations (Dopita & Evans 1986; Edmunds & Pagel 1984; McCa et al. 1985). These analytic $R_{23}$-metallicity relations roughly bracket the range of metallicities that we derive, showing that our measurements are in line with previous strong-line calibrations. However, recent work suggests that strong-line methods may overestimate oxygen abundances systematically by as much as a factor of 2 (Kennicutt et al. 2003).

The strength of our Bayesian metallicity estimates is that they make use of all of the available nebular lines rather than...
relying on a small subset of them, as is the case for $R_{23}$. However, full spectral modeling is not always possible or practical. Hence, we provide an analytical fit to the $R_{23}$-metallicity relation shown in Figure 3:

$$12 + \log (O/H) = 9.185 - 0.313x - 0.264x^2 - 0.321x^3,$$

(1)

where $x \equiv \log R_{23}$. This formula is valid for the upper branch of the double-valued $R_{23}$-abundance relation. The lower branch is not very well sampled by our data. We measure metallicities below $12 + \log (O/H) = 8.5$ for 940 galaxies. However, less than $\frac{1}{4}$ of these can be plotted in Figure 3 because most are at such low redshift that [O ii] $\lambda$3727 is not in our spectroscopic bandpass. While galaxies lacking [O ii] have larger errors associated with their derived abundances, they show trends between abundance and luminosity that are generally consistent with the rest of the sample.

3.2. Measuring Stellar Mass

The stellar mass of a galaxy cannot be inferred directly from its optical luminosity because the stellar mass-to-light ratio depends strongly on the galaxy’s star formation history and metallicity. Optical colors have been widely used to estimate $M/L$ ratios (e.g., Bell & de Jong 2001; Brinchmann & Ellis 2000). However, errors in the derived $M/L$ are known to result if galaxies have formed a substantial fraction (>10%) of their stars in a recent burst. This caveat is particularly problematic given our sample of actively star-forming galaxies. We therefore adopt the method of Kauffmann et al. (2003a) for deriving stellar masses. This method relies on spectral indicators of the stellar age and the fraction of stars formed in recent bursts. As our present sample is actually an extension of Kauffmann’s, we provide only a cursory description of our methods here.

We use the z-band ($\lambda \sim 8900$ Å) magnitude to characterize the galaxy luminosity because it is less sensitive than the bluer bands to extinction and the age of the stellar population. However, even in this near-infrared passband the $M/L$ ratio is not a constant but can vary by up to a factor of 10 when a full range of star formation histories is considered (Kauffmann et al. 2003a; see their Fig. 4). Constraints on the star formation history are provided by the spectral indices $D_\alpha(4000)$ and H$\delta_A$, which measure the 4000 Å break and the stellar Balmer absorption. The location of a galaxy in the $D_\alpha(4000)$-H$\delta_A$ plane is insensitive to reddening and only weakly dependent on metallicity; however, it is a powerful diagnostic of whether the galaxy has been forming stars continuously or in bursts over the past 1–2 Gyr. We assign stellar $M/L$ ratios to our galaxies by using a Bayesian analysis to associate the observed $D_\alpha(4000)$ and H$\delta_A$ values with a model drawn from a large library of Monte Carlo realizations of galaxies with different star formation histories and metallicities. A comparison with broadband photometry then yields estimates of the dust attenuation and the stellar mass. Errors in our masses are estimated from the width of the likelihood distribution. The median 1σ error for our sample of star-forming galaxies is 0.09 dex. Our masses assume a Kroupa (2001) initial mass function (IMF).

4. THE LUMINOSITY-METALLICITY RELATIONSHIP

Because of the relative difficulty of measuring the stellar mass of galaxies, most previous work has focused on the relationship between galaxy luminosity and metallicity. Following the pioneering work of Lequeux et al. (1979), Skillman et al. (1989) established a luminosity-metallicity relation for irregular galaxies that was confirmed by Richer & McCall (1995) and extended to spiral galaxies by Garnett & Shields (1987), Vila-Costas & Edmunds (1992), Zaritsky et al. (1994), and Kobulnicky & Zaritsky (1999). Recently attempts have been made to provide better comparison samples for high redshift by studying the luminosity-metallicity relation in starburst nuclei (Coziol et al. 1997), UV-selected galaxies (Contini et al. 2002), emission-line–selected galaxies (Melbourne & Salzer 2002), and large magnitude-limited samples (Lamareille et al. 2004). It is instructive to compare the luminosity-metallicity relation of our sample with previous work, both to validate the consistency of our measurements and to elucidate the effects of our sample selection. Although redder bandpasses are less sensitive to the effects of dust obscuration and recent starbursts, historical precedent mandates that the luminosity-metallicity relationship be presented in terms of absolute $B$ magnitude. Fortunately, the SDSS $g$ band is fairly similar to the Johnson $B$ band. We adopt the transformation given in Smith et al. (2002) and k-correct the magnitudes to $z = 0$ using the $kcorrect$ code of Blanton et al. (2003b). We correct our measured blue luminosities for Galactic foreground extinction (Schlegel et al. 1998) and for inclination-dependent intrinsic attenuation (Tully et al. 1998). The latter implies a correction to a face-on orientation but does not account for the intrinsic attenuation in a face-on system. The median correction is $A_B^{inc} = 0.3$ mag.\(^\text{14}\)

Figure 4 shows the luminosity-metallicity relation of the SDSS galaxies and various samples from the literature. We

\(^{14}\)Note that the inclination-dependent attenuation correction of Tully et al. (1998) includes a luminosity-dependent term. However, this does not have a significant impact on the slope of the luminosity-metallicity relation. Without the inclination-dependent correction the fitted relation is $12 + \log (O/H) = -0.186 M_B + 5.276$.\n
4.—Luminosity-metallicity relation for SDSS galaxies and various galaxy samples drawn from the literature (see legend). All of the $B$ magnitudes have been corrected to $H_0 = 70$ km s$^{-1}$ Mpc$^{-1}$, but we have made no attempt to homogenize the metallicity measurements. The red line represents the linear least-squares bisector fit to the SDSS data. The inset plot shows the residuals of the fit.
have corrected the published $B$-band luminosities to our adopted value of $H_0$ where appropriate, but we have made no attempt to homogenize the metallicities to account for the different calibrations used. In comparing SDSS data with other samples, it is important to consider the possible aperture bias. We expect our metallicity measurements to slightly overestimate the true global abundances, as discussed further in § 7. However, in view of the different metallicity calibrations used, the magnitude of this offset is probably not the dominant systematic effect. The SDSS data show generally good agreement with other local samples of galaxies, albeit with a paucity of dwarfs.

In keeping with previous work, we fit the luminosity-metallicity relation using a linear least-squares technique. The measurement errors in luminosity ($\pm 0.01$ dex) and metallicity ($\pm 0.1$ dex) are small compared to the observed scatter. The traditional method of estimating the underlying functional relation in this case is to use the linear bisector, the line that bisects the ordinary least-squares regression of $X$ versus $Y$ and $Y$ versus $X$ (Isobe et al. 1990). The luminosity-metallicity relation for our galaxies fitted in this manner is

$$12 + \log (O/H) = -0.185(\pm 0.001)M_B + 5.238(\pm 0.018).$$

(2)

Our measured slope is intermediate between that found by Kobulnicky & Zaritsky (1999) for local irregulars and spirals and that measured by Melbourne & Salzer (2002) for a subset of galaxies from the KPNO International Spectroscopic Survey (KISS). In intercomparing data sets it is important to note that different authors (including the two mentioned above) have adopted different regression methods. Different regression methods calculate intrinsically different properties of the data and are not directly comparable (see Isobe et al. 1990 for a full discussion). Figure 4 therefore elucidates the differences in the measured luminosity-metallicity relation that are the result of sample selection, metallicity calibration, and data characterization (fitting). All of these factors need to be carefully considered when looking for evidence of evolution in the luminosity-metallicity relation.

At fixed metallicity, the SDSS galaxies span more than 4 mag in blue luminosity. The brightest galaxies are consistent with the luminosity-metallicity relation found by Contini et al. (2002) for a sample of UV-selected galaxies (Fig. 4, pink line). Contini et al. (2002) postulate that these galaxies are offset from the luminosity-metallicity relation of normal spirals owing to the low $M/L$ ratio of their newly formed stellar populations. This suggests a physical origin for the scatter, an idea that we explore further in Figure 5. To reduce sources of measurement error, we switch to using the luminosity in the native SDSS passbands, $k$-corrected to the median redshift, $z \sim 0.1$. To quantify the influence of dust, we correct the galaxy luminosities for intrinsic attenuation using the attenuation curve of Charlot & Fall (2000) and assuming that the stars experience $\frac{1}{3}$ of the attenuation measured in the nebular gas. The nebular attenuation is determined simultaneously with the metallicity assuming a metallicity-dependent case B $\text{H}_\alpha/\text{H}\beta$ ratio (Brinchmann et al. 2004; S. Charlot et al. 2004, in preparation). We assume that the correction for intrinsic attenuation automatically accounts for any inclination-dependent effects.

In Figure 5 we systematically examine the impact of dust and $M/L$ variations on the luminosity-metallicity relation by adopting different measures of galaxy luminosity: (1) the absolute $g$-band magnitude corrected for inclination-dependent attenuation following Tully et al. (1998); (2) the absolute $g$-band magnitude corrected for intrinsic attenuation, as described above; and (3) the absolute $z$-band magnitude corrected for intrinsic attenuation. In the top left, top right, and bottom left panels of Figure 5 we indicate the distribution of metallicity at a given luminosity by displaying the contours that enclose 68% and 95% of the data in bins of 0.4 mag. The contours provide a nonparametric description of the distribution, which is unbiased as long as the errors in luminosity are small relative to our adopted bin size. For comparison, we also show the traditional least-squares linear bisector fit to the data in the top left panel [12 + log $(O/H) = -0.186(\pm 0.001)M_g + 5.195(\pm 0.018)$]. Because we do not know a priori the true functional form of the luminosity-metallicity relation, we focus on the contours. Data for the contours in the left panels of Figure 5 are given in Tables 1 and 2.

Comparison of the top two panels of Figure 5 shows that correcting the luminosity for attenuation reduces the scatter and flattens the luminosity-metallicity relation at high mass. This trend is even more pronounced when the extinction-corrected $z$-band magnitude is used (bottom left panel). Because the $z$ band is less sensitive to dust and recent starbursts, the range of $M/L$ ratios is smaller, and the scatter is reduced by $\sim 20\%$ compared to the uncorrected $g$ band. However, even in the $z$ band, $M/L$ ratios can vary by factors of a few. This effect is illustrated in the bottom right panel where we plot the median $z$-band luminosity-metallicity relation for galaxies in four bins of $D_d(4000)$. As discussed in Kauffmann et al. (2003a), $D_d(4000)$ is a good measure of the mean stellar age of the population. Our interpretation of the bottom right panel is that at fixed metallicity, galaxies with lower $D_d(4000)$ are shifted to brighter magnitudes because of the lower $M/L$ ratios of their young stellar populations. This confirms our intuition that the underlying physical correlation is between stellar mass and metallicity.

5. THE MASS-METALLICITY RELATIONSHIP

With our new prescriptions for measuring stellar mass and gas-phase metallicity it is now possible to examine the mass-metallicity relationship of our sample of SDSS star-forming galaxies. Figure 6 shows that a striking correlation is observed, extending over three decades in stellar mass and a factor of 10 in metallicity. The correlation is roughly linear from $10^{8.5}$ to $10^{10.5} M_\odot$, after which a gradual flattening occurs. Most remarkable of all is the tightness of the correlation: the 1 $\sigma$ spread of the data about the median is $\pm 0.10$ dex, with only a handful of extreme outliers present. The relationship is well fitted by a polynomial of the form

$$12 + \log (O/H) = -1.492 + 1.847(\log M_*) - 0.08026(\log M_*)^2,$$

(3)

where $M_*$ represents the stellar mass in units of solar masses. This equation is valid over the range $8.5 < \log M_* < 11.5$. Data on the metallicity distribution at fixed stellar mass are provided in Table 3.

The principal difference between the mass-metallicity and luminosity-metallicity relations is the more pronounced turnover seen at high metallicity when mass is used as the independent variable. In Figure 5 we demonstrated that both dust and $M/L$ variations act to smear out the turnover when luminosity is used in place of mass. Accordingly, the scatter in the
uncorrected $g$-band luminosity-metallicity relation is $\sim 50\%$ higher than the scatter in the mass-metallicity relation. We emphasize that the turnover in the mass-metallicity relation is not an artifact of our metallicity calibration. As shown in Figure 3, our metallicity estimates are consistent with other strong-line calibrations. If we adopt the $R_{23}$ metallicity calibration of Zaritsky et al. (1994), the shape of the mass-metallicity relation is well reproduced, but the scatter increases by $\sim 15\%$. Use of the McGaugh (1991) $R_{23}$ metallicity calibration results in a more pronounced turnover, as a result of the flatter relation between $R_{23}$ and log (O/H).

The shape of the mass-metallicity relation is also robust with respect to our choice of S/N cuts. The S/N in the H$\beta$ line is generally the parameter that drives our galaxy selection. The main concern is that our requirement of $(S/N)_{H\beta} > 5$ may bias us toward massive galaxies with abnormally high gas fractions. However, at fixed equivalent width (EW) the distribution of S/N values is broad. Galaxies with H$\beta$ EW $< 5$ Å have a median $(S/N)_{H\beta}$ of 11, and more than 10% of them have $(S/N)_{H\beta} > 20$. Thus, our cuts on S/N are not imposing stringent cuts on EW or gas fraction. We have also done the straightforward experiment of altering the S/N cuts on all our lines and refitting the mass-metallicity relation: its detailed shape is insensitive to factor of 2 changes in our S/N cuts.

### Table 1

The $g$-Band Luminosity-Metallicity Relation

| $M_g$ | $P_{2.5}$ | $P_{16}$ | $P_{50}$ | $P_{95}$ | $P_{97.5}$ |
|-------|-----------|----------|----------|----------|------------|
| $-22.37$ | $8.86$ | $8.99$ | $9.09$ | $9.15$ | $9.26$ |
| $-21.99$ | $8.88$ | $9.00$ | $9.09$ | $9.15$ | $9.24$ |
| $-21.61$ | $8.87$ | $8.99$ | $9.07$ | $9.14$ | $9.23$ |
| $-21.23$ | $8.84$ | $8.97$ | $9.07$ | $9.14$ | $9.23$ |
| $-20.84$ | $8.77$ | $8.92$ | $9.04$ | $9.13$ | $9.21$ |
| $-20.45$ | $8.71$ | $8.87$ | $9.01$ | $9.11$ | $9.19$ |
| $-20.05$ | $8.66$ | $8.82$ | $8.97$ | $9.09$ | $9.17$ |
| $-19.67$ | $8.60$ | $8.76$ | $8.93$ | $9.07$ | $9.17$ |
| $-19.26$ | $8.55$ | $8.71$ | $8.89$ | $9.05$ | $9.16$ |
| $-18.87$ | $8.39$ | $8.64$ | $8.83$ | $9.02$ | $9.14$ |
| $-18.46$ | $8.32$ | $8.61$ | $8.81$ | $9.00$ | $9.14$ |
| $-18.07$ | $8.21$ | $8.52$ | $8.70$ | $8.96$ | $9.11$ |
| $-17.68$ | $8.20$ | $8.41$ | $8.66$ | $8.89$ | $9.12$ |
| $-17.28$ | $8.18$ | $8.34$ | $8.62$ | $8.87$ | $9.07$ |
| $-16.87$ | $8.08$ | $8.23$ | $8.49$ | $8.81$ | $9.15$ |

Notes.—The columns labeled $P$ represent the 2.5, 16, 50, 84, and 97.5 percentile of the distribution of metallicity in bins of 0.4 dex in luminosity. $P_{50}$ is the median. The $g$-band luminosity is in AB magnitudes and has been corrected for inclination-dependent extinction but not internal extinction.
more of the disk is seen in projection in our fiber aperture at higher inclinations. The integrated metallicity decreases as larger galaxy radii are probed because the outer regions of disks tend to be more metal-poor, as well as more gas-rich and less extincted.

6. THE ORIGIN OF THE MASS-METALLICITY RELATION

The existence of a tight (±0.1 dex) correlation between stellar mass and metallicity reflects the fundamental role that galaxy mass plays in galactic chemical evolution. However, it is not a priori clear whether this sequence is one of enrichment or of depletion. Simply put, if more massive galaxies form fractionally more stars in a Hubble time than their low-mass counterparts, then the observed mass-metallicity relation represents a sequence in astration. However, if galaxies form similar fractions of stars, then the relation could imply that metals are selectively lost from galaxies with small potential wells via galactic winds.

Both of these ideas have a long history in the astronomical literature. It is well known that there are systematic trends in the star formation history of galaxies along the Hubble sequence (e.g., Roberts & Haynes 1994). Recent observations have confirmed that gas mass fractions decrease with increasing stellar mass (McGaugh & de Blok 1997; Bell & de Jong 2000; Boselli et al. 2001), a trend that seems to suggest that low-mass galaxies are unenriched compared to their high-mass counterparts, then the observed mass-metallicity relation represents a sequence in astration. However, if galaxies form similar fractions of stars, then the relation could imply that metals are selectively lost from galaxies with small potential wells via galactic winds.

The effects of astration and mass loss on the relationship between mass and metallicity can be disentangled in principle if information on the relative mass of the gas and stars is available. Simple closed box chemical evolution models predict that metallicity (Z) is a simple function of the stellar yield, y, and of the gas mass fraction, μgas:

\[ Z = y \ln \left( \frac{\mu_{\text{gas}}}{\mu_{\text{gas}}^0} \right). \]

Following Garnett (2002), we assume that the stellar yield is constant. Metallicity is then straightforwardly related to the gas mass fraction if the tenets of the simple model apply, namely, that there are no gas inflows or outflows. We can invert equation (1) to define the “effective yield,” which can be computed from the observed metallicity and gas mass fraction. When the simple model applies, the effective yield will equal the true yield, independent of galaxy mass. This straightforward observational test was performed by Garnett (2002) using a sample of 44 nearby spiral and irregular galaxies. Garnett found the effective yield to be constant for galaxies with rotational velocities in excess of \( \sim 150 \) km s\(^{-1}\) and to decline by a factor of \( \sim 15 \) below this threshold.

While our SDSS data set is much larger than the nearby sample of Garnett, we do not have direct information about the H I and H\(_2\) gas content of our galaxies. However, we do have indirect information, by virtue of the fact that all of our sample galaxies are actively forming stars. To estimate the gas...
mass, we invoke another well-known empirical correlation, the Schmidt star formation law (Schmidt 1959; Kennicutt 1998), which relates the star formation surface density to the gas surface density.

For each of our galaxies we calculate the star formation rate (SFR) in the fiber aperture from the attenuation-corrected Hα luminosity following Brinchmann et al. (2004). We multiply our SFRs by a factor of 1.5 to convert from a Kroupa (2001) IMF to the Salpeter IMF used by Kennicutt (1998). Our SDSS galaxies have star formation surface densities that are within a factor of 10 of $\Sigma_{\text{SFR}} = 0.3 M_\odot \text{yr}^{-1} \text{kpc}^{-2}$, exactly the range found by Kennicutt (1998) for the central regions of normal disk galaxies. We convert star formation surface density to surface gas mass density, $\Sigma_{\text{gas}}$, by inverting the composite Schmidt law of Kennicutt (1998),

$$\Sigma_{\text{SFR}} = 1.6 \times 10^{-4} \left( \frac{\Sigma_{\text{gas}}}{1 M_\odot \text{pc}^{-2}} \right)^{1.4} M_\odot \text{yr}^{-1} \text{kpc}^{-2}. \quad (5)$$

(Note that the numerical coefficient has been adjusted to include helium in $\Sigma_{\text{gas}}$.) Combining our spectroscopically derived M/L ratio with a measurement of the z-band surface brightness in the fiber aperture, we compute $\Sigma_{\text{star}}$, the stellar surface mass density. The gas mass fraction is then $\mu_{\text{gas}} = \Sigma_{\text{gas}} / (\Sigma_{\text{gas}} + \Sigma_{\text{star}})$.

In Figure 8 we plot the effective yield of our SDSS star-forming galaxies as a function of total baryonic (stellar+gas) mass. Baryonic mass is believed to correlate with dark mass, as evidenced by the existence of a baryonic “Tully-Fisher” relation (McGaugh et al. 2000; Bell & de Jong 2001). We are interested in the dark mass because departures from the “closed box” model might be expected to correlate with the depth of the galaxy potential well. Data on the distribution of the effective yield at fixed baryonic mass are provided in Table 4. Because very few of our SDSS galaxies have masses below $10^{8.5} M_\odot$, we augment our data set with measurements from Lee et al. (2003), Garnett (2002), and Pilyugin & Ferrini (2000), all of which use direct gas mass measurements. We
note that the correspondence between the SDSS data and the samples from the literature is very good in spite of the fact that the gas masses have been determined in very different ways.

With the addition of the data from the literature it is clear that galaxies do not evolve as "closed boxes." Figure 8 shows that baryonic mass and effective yield are highly correlated, with the effective yield decreasing by a factor of ~10 from the most massive galaxies to dwarfs. The correlation is steep at lower redshifts, with the effective yield decreasing by a factor of ~3 at redshifts of z = 0.15 dex in stellar mass.

### TABLE 3

| $\log (M_c/Z_\odot)$ | $P_{2.5}$ | $P_{16}$ | $P_{50}$ | $P_{84}$ | $P_{97.5}$ |
|----------------------|-----------|----------|----------|----------|------------|
| 8.57                 | 8.18      | 8.25     | 8.44     | 8.64     | 8.77       |
| 8.67                 | 8.11      | 8.28     | 8.48     | 8.65     | 8.84       |
| 8.76                 | 8.13      | 8.32     | 8.57     | 8.70     | 8.88       |
| 8.86                 | 8.14      | 8.37     | 8.61     | 8.73     | 8.89       |
| 8.96                 | 8.21      | 8.46     | 8.63     | 8.75     | 8.95       |
| 9.05                 | 8.26      | 8.56     | 8.66     | 8.82     | 8.97       |
| 9.16                 | 8.37      | 8.59     | 8.68     | 8.82     | 8.95       |
| 9.26                 | 8.39      | 8.60     | 8.71     | 8.86     | 9.04       |
| 9.36                 | 8.46      | 8.63     | 8.74     | 8.88     | 9.03       |
| 9.46                 | 8.53      | 8.66     | 8.78     | 8.92     | 9.07       |
| 9.57                 | 8.59      | 8.69     | 8.82     | 8.94     | 9.08       |
| 9.66                 | 8.60      | 8.72     | 8.84     | 8.96     | 9.09       |
| 9.76                 | 8.63      | 8.76     | 8.87     | 8.99     | 9.10       |
| 9.86                 | 8.67      | 8.80     | 8.90     | 9.01     | 9.12       |
| 9.96                 | 8.71      | 8.83     | 8.94     | 9.05     | 9.14       |
| 10.06                | 8.74      | 8.85     | 8.97     | 9.06     | 9.15       |
| 10.16                | 8.77      | 8.88     | 8.99     | 9.09     | 9.16       |
| 10.26                | 8.80      | 8.92     | 9.01     | 9.10     | 9.17       |
| 10.36                | 8.82      | 8.94     | 9.03     | 9.11     | 9.18       |
| 10.46                | 8.85      | 8.96     | 9.05     | 9.12     | 9.21       |
| 10.56                | 8.87      | 8.98     | 9.07     | 9.14     | 9.21       |
| 10.66                | 8.89      | 9.00     | 9.08     | 9.15     | 9.23       |
| 10.76                | 8.91      | 9.01     | 9.09     | 9.15     | 9.24       |
| 10.86                | 8.93      | 9.02     | 9.10     | 9.16     | 9.25       |
| 10.95                | 8.93      | 9.03     | 9.11     | 9.17     | 9.26       |
| 11.05                | 8.92      | 9.03     | 9.11     | 9.17     | 9.27       |
| 11.15                | 8.94      | 9.04     | 9.12     | 9.18     | 9.29       |
| 11.25                | 8.93      | 9.03     | 9.12     | 9.18     | 9.29       |

Notes.—The columns labeled $P$ represent the 2.5, 16, 50, 84, and 97.5 percentile of the distribution of metallicity in bins of 0.1 dex in stellar mass. $P_{50}$ is the median.

The free parameters of the fit are $y_0$, the true yield (if no metals are lost), and $M_0$, the mass at which a galaxy loses $\frac{1}{4}$ of its metals. We perform the fit to a combination of the SDSS data (the median value of $y_{\text{eff}}$ in bins of 0.1 in $M_{\text{baryon}}$) and the data drawn from the literature, applying weights such that both data sets contribute equally to the fit. We find $y_0 = 0.0104$ and $M_0 = 3.67 \times 10^9 M_\odot$. This characteristic mass corresponds to a rotation speed of $V_c = 85 \text{ km s}^{-1}$ and, following Heckman et al. (2000), an escape velocity of $V_{\text{esc}} \sim 2V_c = 260 \text{ km s}^{-1}$. Thus, the escape velocity of a galaxy that has lost half of its metals is just below the observed terminal velocity of starburst winds, which are 300–900 km s$^{-1}$ (Heckman et al. 2000).

The scatter in the correlation between effective yield and baryonic mass is ±0.15 dex, 50% larger than that measured for the mass-metallicity relation. However, much of the scatter in the SDSS data can probably be ascribed to our relatively uncertain measurement of the gas mass. We note that this does not effect the total mass greatly, as the median gas mass fraction of our sample is ~20%. It is interesting to note that galaxies with direct gas mass measurements show comparable scatter; however, the stellar mass determinations for these galaxies are correspondingly more uncertain. It is therefore premature to consider a physical origin for the scatter, although it is quite likely that there may be one, for instance, differences in galaxy environment (Skillman et al. 1996; Lee et al. 2003).

### 7. SOURCES OF SYSTEMATIC ERROR

Galaxies are known to have radial gradients in their physical properties (e.g., Bell & de Jong 2000). Aperture effects are therefore a potentially serious concern because strong selection effects are inherent in magnitude-limited surveys such as the SDSS. For our sample, the median projected fiber size is ~4.6 kpc in diameter, with the range extending from 1 to 12 kpc. Thus, while we are not measuring “nuclear” spectra, we are clearly not measuring integrated spectra either. The median fraction of galaxy light in the fiber aperture is 24%. Fortunately, because larger galaxies are brighter, they get selected out to larger distances and observed with larger projected apertures. The net effect is that the fraction of galaxy light seen by the fibers is not a strong function of absolute magnitude, as shown in the top panel of Figure 9. Hence, while aperture effects are important in the absolute sense, they are unlikely to have a significant effect on trends with galaxy mass.

Because of the magnitude-limited nature of the SDSS, it is not possible to examine the impact of aperture size simply by comparing galaxies in narrow bins of absolute magnitude at different redshifts. Instead, we divide our sample into four broad bins of absolute magnitude and examine trends in galaxy properties as a function of relative redshift, $z/z_{\text{max}}$, where $z_{\text{max}}$ is the redshift at which a given galaxy reaches the spectroscopic survey limits. The effect of aperture bias on galaxy M/L ratios was examined as a function of $z/z_{\text{max}}$ by Kauffmann et al. (2003a; see their Fig. 18) and found to be ~0.1 dex. The strongest trends were observed for L$^*$ galaxies, which presumably have both a well-developed bulge and a disk. The effect of aperture bias on our measured metallicity is shown in Figure 9. We find a change of at most ~0.11 dex in metallicity as galaxies move from one edge of the survey to the other, indicating that our metallicity determinations are only moderately affected by changes in the projected aperture size. This gradient is in good accord with our expectations based on the known radial metallicity gradients in spiral galaxies.
While it is desirable to correct our metallicity measurements to reflect true global abundances, it is not possible to derive this correction directly from the SDSS data because even at the limits of the survey the fiber aperture only contains about 50% of a galaxy’s light. Work is under way to obtain the observations necessary for such an analysis. In the meantime, we simply note that because the fibers generally cover the inner few kiloparsecs of galaxies, the abundances we derive are likely to be higher than true integrated abundances. Recent evidence also suggests that oxygen abundances derived from “strong-line” methods like ours may overestimate the true abundance by as much as a factor of 2 (Kennicutt et al. 2003).

Another potential source of error is our indirect method of deriving the gas mass from the Hα luminosity via the global Schmidt law of Kennicutt (1998). While the impressive correlation between the surface mass density of gas and the surface density of star formation holds over 5 orders of magnitude, there is a fair amount of scatter evident in the narrow regime applicable to the present study (Kennicutt 1998; see their Fig. 6). Systematic errors are a bigger concern. Wong & Blitz (2002) found that application of a radially dependent attenuation correction to Hα produced a steeper
Schmidt law, with a power-law index of 1.7 (as compared to Kennicutt’s 1.4). However, adopting the steeper Schmidt law in our analysis produces a relatively small change in the correlation between baryonic mass and effective yield: log $y_0$ decreases by 0.04 dex, and log $M_0$ decreases by 0.15 dex.

Beyond the issue of the accuracy of our $\mu_{gas}$ measurement, there is the larger question of whether the central gas mass fraction is the relevant gas mass fraction. If $\Sigma_{gas}/\Sigma_{star}$ varies strongly with radius, then our measurements are unlikely to be representative of the galaxy as a whole. These concerns are allayed to some degree by the generally strong correspondence seen between $H\alpha$ and broadband optical disk scale lengths (Hodge & Kennicutt 1983; Kennicutt 1989). A more fundamental question, however, is how the products of star formation are distributed in galaxies; in other words, how well mixed is the ISM? The mere existence of radial metallicity gradients in spirals suggests that mixing timescales are generally long. In this case, local abundances reflect local astration levels, and hence the relevant gas mass fraction is the local one. A final issue is the existence of cold gas external to the stellar disk in some galaxies. It is unclear whether this gas is relevant to our calculation, since it does not strongly participate in the star formation. However, if the outlying gas viscously mixes with gas in the inner disk, it would affect the observed metallicity and should be included in the gas budget. In any case, since we have no information on the extended gas in our galaxies, we do not consider it at present, except to note that its inclusion would raise our measured value of the effective yield. For galaxies with baryonic masses of $10^7 M_\odot$, the gas mass would need to increase by a factor of $\sim 11$ to erase the signatures of metal loss.

While the sources of systematic error cannot be ignored, we believe the magnitude of these errors to be small, on the order of a few tenths of a dex. In view of the moderately large

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**Fig. 8.—** Effective yield as a function of total baryonic mass (stellar+gas mass) for 53,400 star-forming galaxies in the SDSS. The large black filled diamonds represent the median of the SDSS data in bins of 0.1 dex in mass that include at least 100 data points. The solid lines are the contours that enclose 68% and 95% of the data. The colored plus signs are data from Lee et al. (2003), Garnett (2002), and Pilyugin & Ferrini (2000). Both the metallicities and the gas masses used to derive the effective yield have been computed differently in the SDSS data and the samples from the literature. The agreement nevertheless appears quite good. The pink line is the best fit to the combined data set assuming the intrinsic functional form given by equation (6). The dashed line indicates $y_0$, the true yield if no metals are lost, derived from the fit to the data. The pink stars denote galaxies that have lost 50% and 90% of their metals. Data for the contours are given in Table 4.
baryonic mass; the percentile of the distribution of the effective yield in bins of 0.1 dex in SDSS data with data from the literature, we find evidence that predict that the effective yield is constant. Combining our effective yield. Simple closed box chemical evolution models lactic winds, an idea first introduced by Larson (1974). Evidence for galactic outflows has steadily accumulated from observations at optical (Lehnert & Heckman 1996; Heckman et al. 2000), X-ray, (Dahlem et al. 1998; Martin et al. 2002), and ultraviolet wavelengths (Heckman & Leitherer 1997; Pettini et al. 2000). However, comparatively little is known about the eventual fate of the wind material—whether it escapes from the galaxy potential or cools and eventually rains back down on the disk. A number of arguments have been made to this effect. Heckman et al. (2000) found the terminal velocity of starburst-driven winds to be 300–900 km s$^{-1}$, independent of the host galaxy properties, and invoked simple models of the gravitational potential to suggest that galactic outflows escape from the potential wells of dwarf galaxies, but not from more massive hosts. However, these simple scaling arguments neglect the multiphase nature of galactic winds and the complicated interaction of the wind with the ISM of the disk and the halo. Drawing on the numerical simulations of Mac Low & Ferrara (1999), which attempt to include this complicated gasodynamics, Ferrara & Tolstoy (2000) conclude that galaxies with gas masses greater than $\sim 10^{10} M_\odot$ do not experience outflows. In contrast, our results imply that galaxies with masses as high as $10^{10} M_\odot$ still eject some fraction of their metals into the intergalactic medium. This result is in line with the recent observational and theoretical work of Strickland et al. (2004). These authors suggest that blowout is possible from galaxies with masses as high as $10^{10} M_\odot$ based on a model where supernovae in disk OB associations work together to power the outflow.

### Table 4

| $\log (M_{\text{baryon}}/M_\odot)$ | $P_{2.5}$ | $P_{16}$ | $P_{50}$ | $P_{94}$ | $P_{97.5}$ |
|----------------------------------|-----------|----------|----------|----------|-----------|
| 8.67                             | -2.84     | -2.74    | -2.57    | -2.34    | -2.08     |
| 8.76                             | -2.75     | -2.69    | -2.52    | -2.32    | -2.05     |
| 8.86                             | -2.80     | -2.68    | -2.51    | -2.27    | -2.03     |
| 8.97                             | -2.74     | -2.60    | -2.39    | -2.18    | -1.98     |
| 9.06                             | -2.72     | -2.60    | -2.40    | -2.21    | -1.98     |
| 9.16                             | -2.73     | -2.53    | -2.35    | -2.17    | -1.98     |
| 9.26                             | -2.69     | -2.49    | -2.31    | -2.13    | -1.92     |
| 9.36                             | -2.65     | -2.46    | -2.30    | -2.12    | -1.93     |
| 9.47                             | -2.61     | -2.43    | -2.27    | -2.11    | -1.95     |
| 9.56                             | -2.56     | -2.39    | -2.24    | -2.08    | -1.89     |
| 9.66                             | -2.55     | -2.38    | -2.24    | -2.09    | -1.90     |
| 9.76                             | -2.49     | -2.35    | -2.21    | -2.06    | -1.90     |
| 9.86                             | -2.50     | -2.33    | -2.19    | -2.04    | -1.87     |
| 9.96                             | -2.46     | -2.32    | -2.18    | -2.03    | -1.87     |
| 10.06                            | -2.44     | -2.30    | -2.17    | -2.02    | -1.85     |
| 10.16                            | -2.44     | -2.29    | -2.15    | -2.01    | -1.83     |
| 10.26                            | -2.43     | -2.27    | -2.13    | -1.99    | -1.82     |
| 10.36                            | -2.43     | -2.26    | -2.12    | -1.98    | -1.80     |
| 10.46                            | -2.41     | -2.25    | -2.11    | -1.96    | -1.80     |
| 10.56                            | -2.38     | -2.23    | -2.09    | -1.94    | -1.78     |
| 10.66                            | -2.38     | -2.22    | -2.07    | -1.93    | -1.77     |
| 10.76                            | -2.36     | -2.21    | -2.07    | -1.92    | -1.78     |
| 10.86                            | -2.36     | -2.21    | -2.06    | -1.91    | -1.77     |
| 10.95                            | -2.36     | -2.20    | -2.05    | -1.90    | -1.75     |
| 11.05                            | -2.38     | -2.20    | -2.05    | -1.90    | -1.74     |
| 11.15                            | -2.36     | -2.19    | -2.04    | -1.88    | -1.70     |
| 11.25                            | -2.38     | -2.20    | -2.03    | -1.86    | -1.73     |
| 11.35                            | -2.30     | -2.18    | -2.01    | -1.82    | -1.68     |

Notes.—The columns labeled $P$ represent the 2.5, 16, 50, 84, and 97.5 percentile of the distribution of the effective yield in bins of 0.1 dex in baryonic mass; $P_{50}$ is the median.
Of course, it is quite likely that even in the absence of winds chemical evolution does not proceed in the simple manner we have assumed. It is worth considering if other factors could explain the trends we observe. For example, another means of lowering the effective yield is the inflow of metal-poor gas. While inflow may occur in some galaxies (the Milky Way, for instance), we do not regard it as a viable explanation for the correlation between effective yield and baryonic mass. Metal-poor inflow acts to lower the metallicity and to raise the gas mass fraction, so the net effect on the effective yield is modest. For example, consider a galaxy presently undergoing closed box chemical evolution with a gas fraction of 0.3. If such a galaxy experiences an inflow of metal-free gas with a mass equal to its present gas mass, the metallicity is reduced by 50%, the gas mass fraction is increased by 54%, and the effective yield is decreased by 22% ($\Delta \log \text{\textit{y}}_{\text{eff}} = 0.1 \text{dex}$). Thus, even dramatic inflow events have only a moderate effect on the effective yield. Garnett (2002) pointed out that the low effective yields of the smallest dwarfs would require them to accrete as much as 80%–90% of their gas at late times without experiencing much star formation. We therefore consider it unlikely that metal-poor inflow is solely responsible for the low yields we observe.

Another factor that can lower the effective yield is a breakdown of the instantaneous recycling approximation, i.e., the assumption that gas is either immediately enriched and returned to the ISM or locked up forever in low-mass stars. While this assumption obviously does not hold in detail, the main practical concern is at late times when low-mass stars return their comparatively unenriched gas to the ISM. If this were a chemically significant effect, then we would expect the effective yield to decrease as a function of mean galaxy age. Kauffmann et al. (2003b; see Fig. 1) demonstrated a tight correlation between stellar mass and the $D_n(4000)$ spectral index, which is a good tracer of the mean stellar age of a population. The correlation is in the sense that more massive galaxies appear to be older. Hence, we would predict that $\textit{y}_{\text{eff}}$ should decrease with galaxy mass, just the opposite of what is seen. While gas recycling may indeed influence the detailed shape of the $\textit{y}_{\text{eff}}$-$M_{\text{baryon}}$ relation, it is almost certainly not the main driver of the observed trend.

It is our view that the strong positive correlation between effective yield and baryonic mass is most naturally explained by the increasing potential barrier that the metal-laden wind must overcome to achieve “blowout.” While the correlation is not particularly tight ($\pm 0.15$ dex), its very existence nevertheless implies two very interesting things. First, nearly all low-mass galaxies and many high-mass galaxies have experienced some sort of blowout event. Since the energy requirements for blowout are fairly exacting, it seems likely that these events are associated with starburst activity. This chain of reasoning leads us to suggest that the star formation histories of most galaxies may be bursty rather than continuous (see, however, Skillman 2001, van Zee 2001, and Hunter & Gallagher 1985 for some opposing viewpoints). Unfortunately, too little is known about the extended gaseous halos of normal galaxies and the conditions required for blowout to make a more quantitative statement (see Strickland et al. 2004). The second significant implication is that blowout events have an important chemical impact even when integrated over a galaxy’s history of star formation. This suggests that blowout is either a very frequent occurrence or very catastrophic. In the coming years numerical and semianalytical models should help to address these questions. In the meantime we emphasize our empirical findings: galactic winds are ubiquitous and extremely effective in removing metals from galaxies.

The quest to understand how the chemical properties of galaxies couple to their star formation histories has been given added impetus of late by measurements of the metallicity-luminosity relation of galaxies at intermediate ($0.3 < z < 1.0$; Kobulnicky et al. 2003; Lilly et al. 2003; Mai et al. 2004) and high ($z > 2$) redshifts (Kobulnicky & Koo 2000; Pettini et al. 2001). Our results imply that metallicity is not a straightforward metric of galaxy evolution because metals can escape galactic potential wells. However, the strong correspondence of metal loss with the size of the potential has interesting implications if effective yields can be measured reliably. The combination of the intermediate- and high-redshift data with the correlations we measure at $z \sim 0.1$ will provide an important benchmark for successful models of feedback and galaxy evolution.

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