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First direct constraints on Fierz interference in free neutron $\beta$ decay

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Precision measurements of free neutron $\beta$-decay have been used to precisely constrain our understanding of the weak interaction. However the neutron Fierz interference term $b_n$, which is particularly sensitive to Beyond-Standard-Model tensor currents at the TeV scale, has thus far eluded measurement. Here we report the first direct constraints on this term, finding $b_n = 0.067 \pm 0.005_{\text{stat}} \pm 0.003_{\text{sys}}$, consistent with the Standard Model. The uncertainty is dominated by absolute energy reconstruction and the linearity of the beta spectrometer energy response.

Precision measurements in nuclear beta decay including lifetimes, angular/spin correlations and energy spectra can be used to test predictions of the electroweak sector of the Standard Model [1–7]. Current efforts are underway to measure many of these quantities in nuclear beta decay as well as in free neutron decay. The Fierz interference term vanishes in the Standard Model but serves as a probe for new physics in scalar and tensor couplings [1, 4]. In this paper, a direct measurement of the Fierz interference term for the free neutron (here denoted $b_n$) is presented for the first time. This term is particularly sensitive to tensor couplings that previous extractions of the Fierz term in superallowed $0^+ \rightarrow 0^+$ beta decay are not.

The Fierz interference term appears in the full form of the differential neutron decay rate parameterized in terms of correlation coefficients of neutron spin, $\bar{\sigma}_n = \bar{J}_n/|\bar{J}_n|$, and momenta, $\bar{p}_e, \bar{p}_\nu$, and total energies, $E_e, E_\nu$, of the final state particles [8]

$$d\Gamma = W(E_e)\left[1 + a \bar{p}_e \cdot \bar{p}_\nu + b_n \frac{m_e}{E_e} + A \bar{p}_e \cdot \bar{\sigma}_n \frac{m_e}{E_e} + B \frac{\bar{p}_\nu \cdot \bar{\sigma}_n}{E_\nu} + \cdots \right] dE_e dE_\nu d\Omega_e d\Omega_\nu,$$

(1)

where $W(E_e)$ includes the total decay rate (e.g. $1/\tau_n$) and the phase space along with recoil-order, radiative and Coulomb corrections. The correlation coefficients also include recoil-order corrections. The dimensionless parameter $b_n$ is the only spin and momentum-direction independent coefficient, and thus survives summation over spin and integration over the final state angular distributions leaving a distribution dependent only on the electron energy, $E$:

$$d\Gamma_b(E) = \left(1 + b_n \frac{m_e}{E}\right) W(E) dE.$$

(2)

For the neutron, a combination of both Fermi and Gamow-Teller components, $b_F$ and $b_{GT}$ respectively, contributes to the Fierz term (see Refs [4, 9]):

$$b_n = \frac{b_F + 3\lambda^2 b_{GT}}{1 + 3\lambda^2}.$$

(3)
where $\lambda \equiv g_A/g_V$ is the ratio of the axial vector to vector nucleon coupling constants. Note that the Fermi and Gamow-Teller components can also be described in terms of an effective field theory (EFT) framework \cite{4,10} that relates new scalar and tensor quark level couplings to $b_{\text{GT}}$ and $b_{\text{GT}}$, respectively.

The best limits for $b_{\text{F}}$ are from a global fit to multiple superallowed $J^z = 0^+ \rightarrow 0^+ \beta$-decay $ft$ values. Hardy and Towner \cite{11} place this limit at $b_{\text{F}} = -0.0028\pm0.0026$, or $|b_{\text{F}}| < 0.043$ at 90% C.L. Several $\beta$ decay experiments have set limits on $b_{\text{CT}}$ using the influence of $b$ on the correlation parameters of Eq. (1) including $^{19}$Ne \cite{12}, $^{60}$Co \cite{13}, $^{114}$In \cite{14}, $^{67}$Cu \cite{15}, and neutrino mass constraints \cite{16}, which give limits in the range $|b_{\text{CT}}| < 0.04—0.13$ at 90% confidence level. These limits are derived from the consistency of the observed correlation coefficient with the Standard Model prediction, assuming $b_{\text{CT}}$ is the dominant Beyond-Standard Model (BSM) contribution. Reviews of limits on tensor contributions in nuclear $\beta$-decay can be found in \cite{2,3,5}. In the EFT approach \cite{4,10} sensitive limits to new tensor couplings, including $b_{\text{CT}}$, can be obtained also from pion decay \cite{17}. While, at present, nuclear beta and pion decays provide the strongest constraints on BSM tensor couplings to left-handed neutrinos \cite{4,5,10}, measurements at the LHC provide the best constraints for tensor couplings to right-handed neutrinos.

For the free neutron, similar limits have been obtained by using the precision correlation parameter $A$ \cite{18,19}. While no measurements of the direct spectral extraction of the Fierz interference term have been published, several precision measurements are underway using $^8$He \cite{20,21} and the free neutron \cite{22}. The sensitivity of these searches is discussed in \cite{23}. Extraction of the Fierz term from measurements of neutron decay has the advantage of the well-understood theoretical treatment of the decay, eliminating the need for nuclear structure corrections which complicate the interpretation of some nuclear decays. In particular, recent reviews such as ref \cite{5}, for example, do not include some (nominally quite stringent) tensor limits from suppressed nuclear decays in which nuclear structure effects hinder the decay relative to strongly allowed decays. Because of its unique characteristics, the UCNA experiment described below, provides an opportunity to directly measure $b_n$ and thus $b_{\text{CT}}$ with comparable precision to nuclear decays.

The ultracold neutron asymmetry (UCNA) experiment is the first experiment \cite{24} to use ultracold neutrons (UCN) in a precision measurement of neutron decay correlations. The 2010 data set from the UCNA experiment provides a precision measurement of the $\beta$ asymmetry parameter, $A$, with a fractional error $< 1\%$ \cite{25}. Because of the $4\pi$ acceptance for the decay electrons, the very low ambient and neutron-generated backgrounds (signal:noise $> 120:1$), and energy reconstruction at the 1% level, this data set also provides a precision measurement of the $\beta$ decay spectrum. This allows, for the first time, a direct spectral extraction of the Fierz interference term, $b_{\text{FT}}$, for the free neutron. Experience with high precision beta decay spectroscopy during the intensive search for a neutrino with 17 keV rest mass for example, highlighted the need for a detailed and quantitative analysis of scattering and energy loss effects for these measurements \cite{26}. Detailed models of the UCNA instrument response over the past ten years of operation allow these effects to be evaluated experimentally and provide a firm foundation for the evaluation of sources of systematic uncertainty in this experiment.

Details of the UCNA experiment are discussed in \cite{9,25,27,28}; here the components of the experiment that allow a measurement of the $\beta$ spectrum are described. A schematic diagram of the UCNA spectrometer is shown in Fig. 1. UCN, generated by the UCN source at the Los Alamos Neutron Science Center \cite{29,30}, are polarized by a 7T superconducting magnet and transported to the copper decay trap centered in the superconducting spectrometer \cite{31} that provides a 1T spin-holding field. UCN are confined by 0.7 $\mu$m thick beryllium-coated mylar foils at the ends of the copper tube decay chamber, trapping UCN while allowing decay electrons to pass through and be transported, via the magnetic field of the spectrometer, to two detectors, located on either end of the decay trap. The magnetic field is reduced in the region of the detectors to 0.6T to reduce backscattering as the incident trajectories are directed more normal to the detector faces while the back scattered events see a magnetic pinch due to the field expansion which reverses the direction for particles scattered well away from normal.

Each detector is composed of a multi-wire proportional chamber (MWPC) \cite{32} and a 3.5 $\mu$m thick plastic scintillator to measure the electron energies. Scintillation light from each detector is directed, via light guides, towards four photomultiplier tubes (PMTs). Gain stabilization is achieved using individual $^{207}$Bi sources embedded in small scintillator blocks attached to each PMT \cite{25,33}. Event triggers require signals above threshold in at least two PMTs and valid events also require a signal in the MWPC. The position measurement done by the MWPC allows a calibration of the position-dependent energy response of the scintillator system (e.g. due to op-
tical transport in the scintillator and light guides) which improves the electron energy reconstruction. This position dependent response is measured by loading the spectrometer with neutron-activated xenon. By observing the decay spectrum features (mainly the 915 keV endpoint from $^{133}\text{Xe}$) as a function of position using the MWPC, the position-dependent light transport of the scintillators is determined. The energy response and linearity of each PMT is calibrated with conversion electron sources ($^{133}\text{Ce}$, $^{116}\text{Sn}$, and $^{207}\text{Bi}$) inserted horizontally, transverse to the spectrometer axis, at different locations across the center of the decay trap. Energy loss due to the sealing foils of each source is determined using a collimated $^{241}\text{Am}$ alpha source and a silicon detector. Overall, the energy response has a low energy threshold of ±60 keV, an energy resolution of 7%/$\sqrt{E}$ (where $E$ is the electron kinetic energy in MeV) dominated by photo-electron statistics and a linearity of ±1%. The uncertainty in the absolute electron kinetic energy varies from ±2.5 keV at 130 keV to ±6.5 keV at 1 MeV.

For the extraction of the $\beta$ decay asymmetry in the UCNA experiment, a super-ratio [25, 27] is formed in terms of the detector efficiencies, $\eta_1$ and $\eta_2$, and the two neutron spin directions. These rates can be written as a product of the spectrum due to the presence of the asymmetry $\sigma$, a “super-sum” is introduced, described in 

\[
\Sigma(E) = \sqrt{\eta_1 \eta_2 N^+ N^- (1 + b_n m_e / E)} W(E). \tag{6}
\]

where, using the rates given in Eq. (4),

\[
\frac{d\Gamma_b(E)}{dE} = \left( \frac{m_e}{E} \right) W(E) \, dE. \tag{7}
\]

while this does not eliminate the detector efficiencies, it does remove dependence on $A$ from the extraction of $b_n$.

For extraction of $b_n$ and for analysis of potential systematic uncertainties, a GEANT4 simulation [34], described in [25, 28], has been modified to include the Fierz term and to incorporate a newer version of GEANT4 (Geant4.10.2)

In the simulation, the 1 T magnetic field of the spectrometer directs electrons towards the detectors on either end, where energy loss in the UCN trap windows, the MWPC and its windows and the plastic scintillator are calculated. The detectors are located in a field expansion region of 0.6T to suppress electron backscattering. A post processor is then used to convert the energy loss into photons, including light quenching via Birk’s Law [35] that was previously calibrated for the UCNA scintillator [36]. This result is then converted into a PMT signal including the effects of energy resolution, due to PMT response shot noise, and low-energy threshold effects.

Two types of initial energy distributions are used for the simulation described above: a pure Standard Model (i.e. $b_n = 0$ in Eq. (2)) and a maximal Fierz distribution in which $\sigma_b = \frac{m_e}{E} W(E) \, dE$.

In both cases the recoil-order, radiative and Coulomb corrections are included (see [28]). Note that these corrections produce a small $m_e/E$ term of order $1 \times 10^{-3}$ [4]. The Fierz term is then extracted by fitting the experimental decay spectrum, $\Sigma(E)$, to a superposition of the Monte Carlo generated Standard Model super-sum and the maximal Fierz super-sum with $b_n$ as a free parameter.

The direct, spectral measurement of $b_n$ is essentially a measurement of a small distortion of the energy spectrum compared to the Standard Model distribution. For example, with a simple allowed phase space spectrum, a $b_n = 0.1$ corresponds to a global shift in the peak of the neutron decay spectrum downward by $\sim 5$ keV. Thus small uncertainties in the energy response (specifically the absolute energy and linearity) can lead to significant systematic uncertainties in the extraction of $b_n$.

In contrast, statistical uncertainties can be quite small for a large data sample. The statistical uncertainties can be estimated using [37] where, assuming $b_n \simeq 0$ and using the full energy spectrum, $\sigma_b = 7.5 / \sqrt{N}$ where $N$ is the number of detected events. Because of detection energy threshold effects, fitting the spectrum at low energies can be problematic. Using a restricted energy range as in [37], and with energy dependent detector efficiency,

\[
\sigma_b^{-2} = m_e^2 N \left( \langle E^{-2} \rangle - \langle E^{-1} \rangle^2 \right), \tag{8}
\]

which, for the electron kinetic energy window used in this work from 150 keV to 650 keV, gives $\sigma_b = 11.4 / \sqrt{N}$. 

An electron energy spectrum that does not have a significant dependence on $A$ can be generated [up to $O (b_n A^2)$] by forming a super-sum as the sum of the geometric means of the spin/detector pairs:

\[
\Sigma(E) = \frac{1}{\sqrt{r_1 r_2}} + \frac{1}{\sqrt{r_2 r_1}}, \tag{5}
\]
Even for this range, with $2.0 \times 10^7$ events from the 2010 UCNA data set, the corresponding statistical uncertainty is $\sigma_\text{stat} < 0.003$, which is much smaller than the systematic uncertainties as described below.

An initial assessment of systematic effects was performed using an analytical model in place of a full simulation [9]. Here the electron energy is generated from the allowed phase space and a model of detector response is used to account for detector efficiency, electron backscattering, background subtraction and energy response effects including energy resolution, non-linearities and absolute energy calibration. These studies indicated relatively modest 1σ systematic uncertainties ($\sigma_b$) from background substractions ($\pm 0.005$), energy resolution ($\pm 0.01$) and electron backscattering from spectrometer windows and detectors ($\pm 0.005$). The small uncertainty due to background subtraction is due to the good signal:noise as discussed in Refs [25, 28]. The backscattering effects are minimized by using events that trigger only one scintillator and its adjacent MWPC. Monte Carlo estimates (which have been benchmarked with detected backscattering events) indicate that only 0.5% of events of this type experience backscattering in the spectrometer windows in front of the detectors. These events experience a small amount of additional energy loss in these windows and are then detected in the opposite detector. The energy dependence of the detector efficiency is estimated to give $\sigma_b \leq 0.02$, assuming an uncertainty of ±20% in the calculated inefficiency. The detector inefficiency due to energy deposition in material along the electron beam path (e.g., detector windows) is determined from the GEANT4 Monte Carlo. The PMT threshold response is determined from the data using overdetermined triggers, since a trigger requires only two PMTs above threshold. We note that the efficiency is > 90% above the minimum energy used for the analysis and the simulated energy deposition is expected to be well-reproduced by the GEANT4 simulation (see [38]). However these analytical studies suggest considerably larger uncertainties ($\geq \pm 0.05$) from non-linearities and absolute energy calibration.

To better quantify the uncertainty due to energy response, the full GEANT4 simulation of the spectrometer is used to investigate how the uncertainty in energy response could contribute to a false $b_n$. As discussed above, this reconstructed kinetic energy response, $E_R$, is determined from a series of calibration runs with conversion electron sources. These sources have an approximately mono-energetic conversion electron with true kinetic energy $E_T$, determined by averaging the individual electron lines over the resolution of the detectors. However this calibration has a corresponding uncertainty [28] due to variations in the detector position response, uncertainties in gain stabilization, etc. These uncertainties are indicated in Fig. 2 for the four energies used in the calibration from the three conversion electron sources. The $E_R$ determined from the calibrations assumes a linear response for conversion of energy deposition to light output after correction for light quenching discussed above. The assumption of linear response is confirmed in Fig. 2 as the observed $\Delta E = E_T - E_R$ is consistent with zero within its uncertainty. These uncertainties are the standard deviation of many global fits to the energy response based on 10-12 separate source location runs taken during each of five separate time periods spread throughout the experiment.

To quantify the systematic uncertainty in $b_n$ due to energy response, Monte Carlo simulations with $b_n = 0$ are performed where the energy response is varied with variations consistent within the uncertainties of $\Delta E$. To do this, the $E_R$ is assumed to be a non-linear polynomial as a function of $E_T$. The coefficients for this polynomial are then sampled in order to reproduce the calibration uncertainties (assumed Gaussian). Both quadratic and cubic polynomials were sampled in separate studies (higher orders are not justified due to the limited impact on $b_n$), but the results are not significantly different. The envelopes for these sampled energy responses
for a quadratic polynomial (both 1σ and 2σ) are shown as bands in Fig. 2. To assess the systematic effects for these varied energy responses, generated energy spectra from each varied response are fit, with $b_n$ as a free parameter, to the Monte Carlo spectrum without varied energy response and $b_n = 0$. The results of the fitted values of $b_n$ for 500 simulated responses are shown in Fig. 3, with the quadratic polynomial assumption. From this distribution a systematic uncertainty due to energy response can be determined for both a 1σ (±0.087) and 90% (±0.104) confidence interval. A summary of the 1σ systematic uncertainties is given in Table I. The experimental decay spectrum $\Sigma(E)$ vs. reconstructed electron kinetic energy is shown in Fig. 4 along with the full Monte Carlo spectrum for $b_n = 0$. The expected spectrum from the Standard Model without energy response is shown as the dashed curve to indicate the effects of detector energy thresholds and energy resolution when compared to the measured spectrum. The lower panel in Fig. 4 shows the shape factor, defined as $(\Sigma_M - \Sigma_{MC})/\Sigma_{MC}$, where $\Sigma_M$ is the measured spectrum and $\Sigma_{MC}$ is the simulated spectrum with $b_n = 0$. A value for the Fierz interference term from the measured data is then determined by fitting the measured shape factor to that expected from Eq. (2). This fit is shown in the lower panel of Fig. 4 as the solid line. Since the systematic uncertainties increase significantly at both low and high energies (i.e. near detector threshold and $\beta$ spectrum endpoint) due to signal:noise degradation and energy response uncertainty, the spectrum is only fitted for electron kinetic energy $150 \text{ keV} < E_R < 650 \text{ keV}$. The fit to the data shows significant disagreement compared to the statistical uncertainties of the measurement likely because of the large systematic uncertainties due to energy response. We note that the statistical uncertainties can be increased by a factor 2.5 to produce a reasonable fit (i.e. $\chi^2 \simeq 1$), but this still leads to a statistical uncertainty much less than the systematic uncertainties discussed above.

The best fit value is $b_n = 0.067 \pm 0.005_{\text{stat}}^{+0.090}_{-0.061_{\text{sys}}}$, where the systematic uncertainty is from the analysis discussed above. This corresponds to a 90% confidence limit interval of $-0.041 < b_n < 0.225$ and, since the error on $b_F$ is much smaller, a similar limit for $b_{GT}$. The result is consistent with a vanishing $b_n$ as predicted by the Standard Model and is dominated by the systematic uncertainty in energy response.

This is the first direct extraction of $b_n$ from a measurement of the decay electron energy spectrum. Future proposed spectral measurements of Fierz interference [7]...
(with sensitivity goals \( \leq 0.005 \)) will require significant improvements in characterization of the energy response of the detection system. More modest improvements in sensitivity to \( b_{GT} \) for UCNA are being investigated via a simultaneous fit to both the spectral and asymmetry \((A)\) energy dependence.

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