Magnetic Ergostars, Jet Formation and Gamma-Ray Bursts: Ergoregions versus Horizons

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We perform the first fully general relativistic, magnetohydrodynamic simulations of dynamically stable hypermassive neutron stars with and without ergoregions to assess the impact of ergoregions on launching magnetically–driven outflows. The hypermassive neutron stars are modeled by a compressible and causal equation of state and are initially endowed with a dipolar magnetic field extending from the stellar interior into its exterior. We find that, after a few Alfvén times, magnetic field lines in the ergostar (star that contains ergoregions) and the normal star have been tightly wound in both cases into a helical funnel within which matter begins to flow outward. The maximum Lorentz factor in the outflow is \(\Gamma_L \sim 2.5\), while the force-free parameter holds at \(B^2/8\pi\rho_0 \lesssim 10\). These values are incompatible with highly relativistic, magnetically-driven outflows (jets) and short \(\gamma\)-ray bursts. We compare these results with those of a spinning black hole surrounded by a magnetized, massless accretion disk that launches a bona fide jet. Our simulations suggest that the Blandford-Znajek mechanism for launching relativistic jets only operates when a black hole is present, though the Poynting luminosity in all cases is comparable. Therefore, one cannot distinguish a magnetized, accreting black hole from a magnetized hypermassive neutron star in the so-called mass-gap based solely on the value of the observed Poynting luminosity. These results complement our previous studies of supramassive remnants and suggest that it would be challenging for either normal neutron stars or ergostars in a hypermassive state to be the progenitors of short \(\gamma\)-ray bursts.

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Introduction.—Event GW170817 [1] marked not only the first direct detection of a binary neutron star (BNS) merger via gravitational waves but also the simultaneous detection of the short \(\gamma\)-ray burst (sGRB) GRB170817A [2, 3], and kilonova AT 2017gfo, with its afterglow radiation in the radio, optical/IR, and X-ray bands. These detections constituted a golden moment in the era of multimessenger astronomy [4–6]. To investigate the different scenarios for jet formation triggering the such electromagnetic (EM) events, fully general relativistic, magnetohydrodynamic (GRMHD) simulations are needed (for recently reviews see e.g. [7–9]).

The most common scenario for launching a magnetically-driven jet is a black hole-disk (BH-disk) remnant. BNS mergers that lead to hypermassive remnants (HMNSs) inevitably collapse to BHs immersed in gaseous disks. These remnants are robust engines for jet launching [10–14]. Their lifetimes are \(\Delta t \approx 150\) ms and outgoing Poynting luminosities \(\sim 10^{52\pm1}\) erg/s, both consistent with typical sGRBs [15–18], as well as with the Blandford-Znajek (BZ) mechanism for launching jets and their associated Poynting luminosities [19, 20]. The key requirement for the emergence of a jet is the existence of a large-scale poloidal magnetic field along the direction of the total orbital angular momentum of the BH-disk remnant [21]. Such a field arises when the NS is initially endowed with a dipolar magnetic field confined or not to the interior of the NSs. During the BNS merger and the HMNS phase, magnetic instabilities drive the magnetic energy to saturation levels [22]. Following the HMNS collapse to a BH, such magnetic fields launch a mildly relativistic, magnetically-driven outflow with a Lorentz factor \(\Gamma_L \gtrsim 1.2\) confined inside a tightly-wound-magnetic funnel. This becomes an “incipient jet” once regions above the BH poles approach force-free values \((B^2/8\pi\rho_0 \gg 1)\). Here \(B\) and \(\rho_0\) are the strength of the magnetic field and the rest-mass density, respectively. For axisymmetric, Poynting-dominated jets, the maximum \(\Gamma_L\) ultimately attained in the funnel is approximately \(B^2/8\pi\rho_0\) [23]. Therefore, incipient jets will become highly relativistic, as required by sGRB models [24].

The possibility of jet launching from a stable NS remnant has recently been investigated [25–27]. In particular, Ref. [25] presented 200 ms-numerical simulations of a stable (supramassive [28]) NS remnant initially threaded by a dipolar magnetic field that extended from the stellar interior into its exterior. Such a stable NS remnant showed no evidence of jet formation, since the outflow confined in the funnel had \(\Gamma_L \lesssim 1.03\) and \(B^2/8\pi\rho_0 \lesssim 1\), thereby lacking a force-free magnetosphere needed for the BZ–like mechanism to power a collimated jet [29]. These results suggest that a supramassive NS remnant, which may arise and live arbitrarily long following the merger of a BNS, probably cannot be the progenitor of a sGRB. These results have been confirmed in Refs. [26, 27], which reported the emergence of a \(\Gamma_L \lesssim 1.05\)-outflow after \(\gtrsim 212\) ms following the merger of a magnetized low-mass BNS. However, it has been suggested that neutrino effects may help reduce the baryon-load in the region above the poles of the NS, which may drive up the force-free parameter in the funnel [30] and lead to jet formation.

Several questions need to be addressed regarding the central engine that launches an incipient jet, as well as the nature of the jet itself. First, the membrane paradigm implies that a spinning BH immersed in a disk is a sufficient condition for jet formation [20, 31], but is it also a necessary condition? If yes, then a stable NS remnant (like a supramassive NS) cannot be the generator of such jets. If no, then is a NS jet qualitatively...
the same as the one launched from BH-disks? In particular, can one still describe it as a BZ-like jet? If not, what are the main differences from a BZ-like jet? It has been argued that contrary to the membrane paradigm, the horizon is not the “driving force” behind the BZ mechanism but rather it is the ergoregion [32–35]. Thus it may be possible that normal NSs cannot launch a BH jet, but ergostars (NSs that contain ergoregions) can. If that is the case, can one distinguish between BH-disk and ergostar jets?

To address the above questions, we employ our recently constructed, dynamically stable ergostars [36, 37] and perform a series of GRMHD simulations that include differentially rotating HMNSs with and without ergoregions to assess the effect of the ergoregion in launching a jet. At the same time, we make critical comparisons between candidate jets and the ones generated by a BH-disk. Our results suggest that an ergoregion does not facilitate or inhibit the launching of outflows. A magnetically-driven outflow with a maximum value of $\Gamma_L \sim 2.5$ is launched whether or not an ergoregion is present (see left column in Fig. 1). This outflow therefore is not consistent with sGRBs, which require flows to reach $\Gamma_L \gtrsim 20$ [24]. In contrast to the BH-disk where the force-free parameter $B^2/8\pi\rho_{0}$ above the BH poles reaches values of $\gtrsim 100$, the force-free parameter in the HMNS cases is only $\lesssim 10$. We find that the Poynting luminosity of our evolved models is comparable to the values reported in [38], as well as to the BZ luminosity. This shows that the value of the luminosity by itself cannot be taken as a criterion to distinguish compact objects with masses in the range $3 - 5 M_\odot$ (the so-called mass-gap). Finally, the angular frequency ratio of the magnetic field lines around the HMNSs is at least twice the value $\Omega_F/\Omega_H \sim 0.5$ expected from the BZ mechanism [39]. Thus our current simulations suggest that the BZ mechanism for launching relativistic jets only operates when a spinning BH is present, and that neither normal NSs nor ergostars can be the central engines that power sGRBs.

**Numerical setup.**—The HMNS initial data are constructed using the GR rotating equilibrium code described in [28] using two equations of state (EOSs). The first one is ALF2cc which was employed in [36] to find the first dynamically stable ergostars. It is based on the ALF2 EOS [40] where the inner region with rest-mass density $\rho_0 \geq \rho_{\text{nuc}} = 2.7 \times 10^{14} \text{ g/cm}^3$ is replaced by $P = \sigma (\rho - \rho_{\text{nuc}}) + P_s$, where $\sigma$ is a dimensionless constant, $\rho$ is the total mass-energy density, and $P_s$ the pressure at $\rho_s$. Here we assume $\sigma = 1$, i.e. a causal core. Since the causal core starts at a relatively low density, $\rho_{\text{nuc}}$, the models based on this EOS have density profiles that resemble the ones found in quark stars which exhibit a finite surface density. The crust of the NS that follows the ALF2cc EOS is about $\% 6$ of the equatorial radius. These models, denoted by NS1 and ES1 in Table I, have been presented in Table I of [36] (with names iA0.2-rp0.47 and iA0.2-rp0.45, respectively). They both belong to the sequence of stars having the same central rest-mass density $\rho_0 = 4.52 \times 10^{14} \text{ g/cm}^3$ and are differentially rotating NSs with a $j$-const rotation law, $j(\Omega) = A^2 (\Omega_c - \Omega)$, where $\Omega_c$ is the angular velocity at the center of the star, and $A = 5$. NS1 has no ergoregion, while the adjacent model ES1, which rotates slightly faster, does.

The second EOS is SLycc2 [37] and is based on the SLy EOS [41] with the interior region having rest-mass density $\rho_0 \geq 2\rho_{\text{nuc}}$ replaced by the same causal EOS as given above. Here the causal core is further from the surface of the star, so a smoother transition to the surface is accomplished. Differentially rotating models with this EOS have been fully explored in [37]. Here we pick two models, NS2 and ES2, that again belong in the sequence of central rest-mass density $\rho_0 = 7.82 \times 10^{14} \text{ g/cm}^3$ and have $A = 3.3$. They are slightly more differentially rotating than the ALF2cc models. Model NS2 has no ergoregion, while the adjacent model ES2 does. Further properties of all our adopted models can be found in Table I. In the following, we consider both pure hydrodynamic and magnetized (MHD) evolutions of these models.

For the magnetized cases, the stars are initially threaded by a dipole-like magnetic field whose strength at the NS poles ranges between $4.5 \times 10^{14} \text{G}$ to $1.5 \times 10^{16} \text{G}$, and with a magnetic dipole moment aligned with the direction of the spin of the star (see top panel of Fig. 3 in [14]). We verify that initially the magnetorotational-instability (MRI) is captured in our models by computing the quality factor $Q_{\text{MRI}} \equiv \lambda_{\text{MRI}}/dx$, which measures the number of grid points per fastest growing (MRI) mode as in [42]. Here $\lambda_{\text{MRI}}$ is the fastest-growing MRI wavelength. We choose astrophysically large magnetic fields to mimic their growth due to the Kelvin-Helmholtz instability (KHI) and the MRI during BNS merger and HMNS formation. These instabilities can amplify moderate magnetic fields ($\sim 10^{13} \text{G}$) to rms values in the HMNS of $\sim 10^{15.5} \text{G}$, and locally up to $\sim 10^{17} \text{G}$ [22, 43, 44]. To capture the magnetosphere that surrounds the NS, we set a variable, low-density magnetosphere in the HMNS exterior such that the plasma parameter $\beta \equiv P_{\text{gas}}/P_{\text{mag}} = 0.01$ everywhere [11]. In all of our cases, the low-density increases the total rest-mass of the star by $\lesssim 1\%$, consistent with the values reported previously (see e.g. [12]). The ideal GRMHD equations are then integrated everywhere, imposing on top of the magnetosphere a density floor in regions where $\rho_{\text{max}} \leq 10^{-10} \rho_{\text{max}}$, where $\rho_{\text{max}}^0$ is the initial maximum rest-mass density of the system.

In addition to the above HMNS models, we evolve a BH-disk of $4 M_{\odot}$ with an initial dimensionless spin $J_{\text{BH}}/M_{\text{BH}}^2 = 0.9$ to match those parameters of models NS2 and ES2 in Table I. The BH is surrounded by a massless accretion disk modeled by a $\Gamma = 4/3$ polytropic EOS which is initially threaded by a pure poloidal magnetic field confined to the disk interior. The maximum value of $\beta$ is $10^{-3}$ (see Eq. 2 in [45]). Since we neglect the self-gravity of the disk, our model can be scaled to an arbitrary rest-mass density and magnetic field, keeping $\beta$ constant (see Eq. A4 in [45]).

We evolve the above systems using the Illinois GRMHD moving-mesh-refinement code (see e.g. [46]), which employs the Baumgarte-Shapiro-Shibata-Nakamura formulation of the Einsteins equations [47, 48] with puncture gauge condi-
TABLE I. Equilibrium models. ER denotes the existence or not of an ergoregion. Parameter $\hat{A} = A/R_e$, where $R_e$, the equatorial radius, determines the degree of differential rotation, $R_p/R_e$ is the ratio of polar to equatorial radius, $M_0$ is the rest mass, $M$ is the ADM mass, $J$ is the ADM angular momentum, $T/|W|$ is the ratio of kinetic to gravitational energy, $P_c$ is the rotation period corresponding to the central angular velocity $\Omega_c$, $\Omega_c/\Omega_s$ is the ratio of the central to the surface angular velocity, and $t_{\text{dyn}} \sim 1/\sqrt{\rho}$ the dynamical timescale.

| Model | EOS     | ER | $\hat{A}^{-1}$ | $R_p/R_e$ | $M_0$ [$M_\odot$] | $M$ [$M_\odot$] | $R_e$ [km] | $J/M^2$ | $T/|W|$ | $P_c/M$ | $\Omega_c/\Omega_s$ | $t_{\text{dyn}}/M$ |
|-------|---------|----|---------------|-----------|------------------|----------------|-----------|---------|---------|--------|----------------|----------------|
| NS1   | ALF2cc  | $\times$ | 0.2          | 0.4688    | 6.973           | 5.587         | 12.55     | 0.8929  | 0.2423  | 25.21  | 1.359            | 6.6             |
| ES1   | ALF2cc  | $\checkmark$ | 0.2        | 0.4531    | 7.130           | 5.709         | 12.49     | 0.9035  | 0.2501  | 24.18  | 1.378            | 6.5             |
| NS2   | SLycc2  | $\times$ | 0.3          | 0.4688    | 4.839           | 3.944         | 8.873     | 0.8666  | 0.2329  | 21.66  | 1.707            | 6.7             |
| ES2   | SLycc2  | $\checkmark$ | 0.3        | 0.4531    | 4.930           | 4.017         | 8.753     | 0.8759  | 0.2403  | 20.58  | 1.743            | 6.6             |

FIG. 1. Final rest-mass density profiles normalized to the initial maximum density (left column) and the force-free parameter inside the helical magnetic funnel (right column) for cases NS2 (top row), ES2 (middle row), and BH-disk (bottom row). White lines depict the magnetic field lines, while the arrows display fluid velocities, and $P_c$ is the rotation period measured at the point where the rest-mass density is maximum. Here $M = 5.9$ km.
tions (see Eq. (2)-(4) in [49]). The MHD equations are solved in conservation-law form adopting high-resolution shock-capturing methods. Imposition of \( \nabla \cdot \vec{B} = 0 \) during evolution is achieved by integrating the magnetic induction equation using a vector potential \( A^x \) [46]). The generalized Lorenz gauge [30] is employed to avoid the appearance of spurious magnetic fields [51]. Pressure is decomposed as a sum of a cold and a thermal part, \( P = P_{\text{cold}} + (\Gamma_{\text{th}} - 1)\rho(\epsilon - \epsilon_{\text{cold}}) \) where \( P_{\text{cold}}, \epsilon_{\text{cold}} \) are the pressure and specific internal energy as computed from the initial data EOS (ALF2cc or SLycc2). For the thermal part we assume \( \Gamma_{\text{th}} = 5/3 \).

In our NS simulations we used nine nested refinement levels with minimum grid spacing (at the finest refinement level) \( \Delta x_{\text{min}} = 122 \text{ m} \) for the ALF2cc models, while for the SLycc2 models, whose radii are much smaller, we used a minimum resolution of \( \Delta x_{\text{min}} = 85.6 \text{ m} \). In both cases the radius of the star is resolved by \( \sim 102 \) grid points. For the BH-disk simulation we used eight refinement levels with \( \Delta x_{\text{min}} = 0.034192k^{3/2} \text{ m} \), where \( k = P^3/\rho_1^2 \) is the polytropic constant in the initial cold disk. The horizon radius is resolved by \( \sim 41 \) grid points.

**Pure hydrodynamic evolutions** — To probe the dynamical stability of models NS2 and ES2, we evolve them following the same procedure as in [36], where the stability properties of models NS1 and ES1 were reported. We find that these models remain in equilibrium for more than a hundred dynamical timescales (\( \gtrsim 30 \) rotation periods). Due to the large density close to the star’s surface, centrifugal forces push the outer layers of the star (low-density layers) slightly outwards, while the bulk of the star remains axisymmetric to a high degree until the end of our simulations (see Fig. 1 in [36]). We do not find evidence of any significant growing instabilities or outflows during this time.

**MHD evolutions** — Magnetically-driven instabilities and winding inevitable change the differential rotation law in the bulk of the stars, and ultimately lead to the transition of the HMNS into another state which may or may not be dynamically stable, depending on the specific characteristics of the initial configuration and the magnetic field. In Fig. 1, the magnetized evolution of the dynamically stable normal star NS2 and ergostar ES2 are shown in the top and middle rows respectively. In both cases after \( 30P_c \) the HMNSs are still differentially rotating, although not in the same way as the initial configurations. To probe the stability of magnetized ergostars and their EM characteristics we survey HMNS models against different magnetic field configurations. Notice that the Alfvén time for magnetic growth in the HMNS (mainly by magnetic winding, followed by MRI) is \( \tau_\alpha \sim 10 \rho_4^{1/4} B_{15}^{-1} R_{10} \text{ms} \) (see Eq. 2 in [21]). Here \( \rho_4 = \rho/10^{14} \text{g/cm}^3 \) is the characteristic density of the HMNS, \( B_{15} = B/10^{15} \text{G} \), and \( R_{10} = R/10^{10} \text{km} \), where \( R \) is the stellar equatorial radius.

The evolutions with the highest magnetic field strength, denoted by NS1-Bh and ES1-Bh, involve the normal HMNS NS1 and ergostar ES1, which as discussed have similar physical properties (see Table I), and a poloidal magnetic field of \( 1.5 \times 10^{16} \text{G} \). We find that after \( \sim \tau_\alpha \sim 3P_c \) magnetic winding and MRI change the rotation law of the HMNSs, driving the onset of stellar collapse. In the ES1-Bh case, the ergoregion expands and after \( 4\tau_\alpha \sim 12P_c \) an apparent horizon appears inside it. A BH horizon in NS1-Bh forms at \( \sim 5\tau_\alpha \sim 15P_c \). Using the isolated horizon formalism [52], we estimate that the BH remnant in both cases has a mass of \( M_{\text{BH}} \approx 0.95M \) and dimensionless spin \( a/M_{\text{BH}} \approx 0.93 \). Here \( M \) is the ADM mass of the corresponding HMNS (see Table I). In both cases the BH is surrounded by an accretion disk with \( \sim 4.2\% \) of the initial HMNS rest mass. The Poynting luminosity (\( L_{EM} \equiv - \int T^{bt}_t \sqrt{-g} dS \)) computed at different extraction radii \( r_{\text{ext}} \gtrsim 80M \) is \( L_{EM} \sim 10^{44} \text{ erg/s} \) for both cases. In the bottom panel of Fig. 2 the ES1-Bh is shown with a solid blue line and the black star symbol marks the BH formation time, and the termination of our simulations. The fate of the BH-disk remnant has been already discussed in [12]; as our initial magnetic field is near saturation, we do not expect additional enhancement following BH formation. However, as the matter above BH poles is accreted onto the BH, the ratio \( B^2/8\pi\rho_0 \) in the funnel will increase up to values \( \gtrsim 100 \), and so the outflow can be accelerated to \( \Gamma_L \gtrsim 100 \) as required by sGRB models [24].

In the medium-magnetized case, ES1-Bm, where \( B = 3 \times 10^{15} \text{G} (\tau_\alpha \sim 13P_c) \), magnetic winding and the MRI slowly drive the star into a new quasistationary configuration, which remains stable for more than \( \sim 30P_c \). We do not find evidence of any significant growing instabilities [36]. During this time, magnetic winding in the bulk of the star induces a linear growth of the toroidal component of the magnetic field and
corresponding magnetic pressure. Alfvén waves then propagate near the rotation axis transporting electromagnetic energy [38]. This builds up magnetic pressure above the stellar poles until eventually the inflow is halted and driven into an outflow confined by the tightly wound field lines. The luminosity for this case is shown in the bottom panel of Fig. 2 with a solid green line. With a solid red line we also show the luminosity of the lowest magnetized case ES1-BI, whose initial magnetic field at the pole is \( B = 4.5 \times 10^{14} \) G.

Similar to the evolution of ES1-Bm, when HMNSS NS2 and ergostar ES2 are threaded by a poloidal magnetic field of \( 5.25 \times 10^{15} \) G (Alfvén time \( \tau_A \sim 12P_c \) ) they evolve stably for more than \( 30P_c \) (top and middle rows of Fig. 1). In both cases, we observe that an outflow is launched after roughly \( \sim 20P_c \) whether an ergoregion is present or not. As shown in Fig. 2 top panel, the corresponding Poynting luminosities are roughly the same, \( L_{\text{EM}} \sim 10^{38} \) erg/s. The comparison between NS2 and ES2 suggest that the ergoregion neither facilitates nor inhibits the launching of a magnetically-driven outflow.

To assess if the BZ mechanism is operating in our systems, we compare the luminosity with that of a BH-disk remnant that launches an incipient jet (right column in Fig. 1). As seen in the top panel of Fig. 2, the luminosity from the BH-disk matches the one coming from the stable HMNSS NS2 and ES2. In the same panel we show with a dashed black line the luminosity predicted by the BZ mechanism: \( L_{\text{BZ}} \sim 10^{51} \frac{a/M_{\text{BH}}}{\Omega_{\text{BH}}^2} (M_{\text{BH}}/4M_\odot)^2 B_{15}^2 (\text{erg/s}) [53, 54] \) for the BH-disk, which is consistent with the numerically computed one. We note here that if one naively applies the same formula to the HMNSS NS2 and ES2 one gets roughly the same results, since the masses, dimensionless spins, and poloidal magnetic fields are the same as those of the BH-disk. The BZ estimates for the cases ES1-Bh, ES1-Bm, and ES1-BI are shown with dashed lines in the bottom panel of Fig. 2 which indicates agreement with the numerical values (solid lines).

In other words, the luminosity is not an efficient diagnostic for distinguishing outflows coming from a BH-disk or those coming from a NS. For example, a magnetized compact object in the mass gap will yield the same luminosity as the BZ formula, making impossible its identification (BH-disk vs HMNSS) through this criterion.

Ref. [38] concludes that HMNSSs like our models emit EM radiation with a luminosity \( L_{\text{EM}} \sim 10^{51} B_{15}^2 R_{10}^5 \Omega_4 \) erg/s, where \( \Omega_4 = \Omega/10^4 \) rad/s. This estimate is shown in both panels of Fig. 2 with dotted lines, and coincide with the BH dashed lines to a very high precision. This is curious, since the two formula exhibit very different scaling with parameters. Both of them are also close to the numerically computed luminosity.

One other possible source of luminosity is the pulsar spin-down luminosity [55], which according to [56] can be enhanced by as much as \( \sim 35\% \) relative to its Minkowski value, if general relativistic effects are taken into account. The numerical values shown in Fig. 2 (as well the BZ estimate and the estimate from Ref. [38]) show that our luminosities are at least one order of magnitude larger than those found in [56]. This is not surprising since: (1) the stars in our recent analysis are differentially rotating, not uniformly rotating, as in [56]. Thus field lines tied to matter on the surface cannot “corotate” with a rigidly rotating surface inside the light cylinder, as in a pulsar, but get wound up due to magnetic winding in the helical pattern we observe and which follows the exterior plasma flow. (2) Our magnetosphere is only marginally force-free, unlike the pulsars modeled in [56], which are strongly force-free. Hence the exterior field topology, which is always attached to the plasma, does not show nearly the same degree of winding under truly force-free conditions and the flow is thus also with less winding. Because of these reasons it is difficult to make a comparison regarding the spin-down luminosity in our simulations. We will address this issue in a future work.

Following [10], we measure the level of collimation of the outflow from the funnel opening angle, which can be determined by the \( B^2/8\pi\rho_0 \sim 10^{-2} \) contour. Based on this value, we estimate an opening angle of \( \sim 25^\circ \) in our HMNS models. Such behavior has already been found in [25] where a HMNS has been evolved for \( \sim 200 \) ms. Similar results have been reported in [27]. This level of collimation, although robust, is not as tight as in the BH-disk where the opening angle is \( \sim 15^\circ \). The existence of the ergoregion does not seem to affect either the development of this funnel structure or its geometry.

In all cases, fluid elements inside the funnel have specific energy \( E = -u_0 - 1 > 0 \) and hence are unbound. The characteristic maximum value of the Lorentz factor is \( \Gamma_L \sim 2.5 \) for cases NS2 and ES2, while \( \Gamma_L \sim 1.3 \) in the BH-disk case. However, the force-free parameter \( B^2/8\pi\rho_0 \) inside the funnel in the latter case is a factor of \( \gtrsim 10 \) larger than that of the HMNS cases (where \( B^2/8\pi\rho_0 \lesssim 10 \)). Since in steady-state the maximum attainable \( \Gamma_L \) of axisymmetric jets equals the plasma parameter [23], only in the BH-disk case material inside the funnel can be accelerated to \( \Gamma_L \gtrsim 100 \) as required for sGRBs [24]. Given the fact that magnetic winding and MRI will further transfer angular momentum to the surface and make these HMNSSs more uniformly rotating, leading to catastrophic collapse, as in case ES1-Bh, we do not expect that further evolution will produce any significant changes until BH formation, given what is shown in the right column of Fig. 1. As the magnetic field is near saturation, the only way for \( B^2/8\pi\rho_0 \) to grow is for the funnel to become baryonfree. However, the outer layers of the star are a repository of matter that constantly supplies appreciable plasma inside the funnel.

Another characteristic of the BZ mechanism is the value \( \Omega_F/\Omega_H \). Here \( \Omega_F = F_t/F_\phi \) is the angular frequency of the magnetic field lines and \( \Omega_H = (a/m)(1 + \sqrt{1 - (a/m)^2})/(2m) \) is the angular frequency of the BH horizon. For a Kerr BH with \( a/m = 0.9 \) in a strongly force-free disk this ratio increases from \( \sim 0.49 \) at the pole to \( \sim 0.53 \) at the equator [57]. Numerical simulations that resulted in successful jet formation [10, 12, 14, 58] have found this ratio to be \( \sim 0.1 - 0.6 \). We find \( \Omega_F/\Omega_H \in [0.2, 0.5] \) when \( \theta \in [0, \pi/2] \) in our present BH-disk simulation. Although this ratio is defined only for BHs, we nevertheless calculate...
its value using the central/surface angular velocity of the neutron star. We find $\Omega_F/\Omega_c \in [0.4, 0.8]$, while if we normalize with the surface angular velocity $\Omega_s$ instead, the ratio $\Omega_F/\Omega_s$ becomes $\sim 1.5$ times larger. These results are approximately the same for both NS2 and ES2 and, therefore, the presence of the ergoregion does not seem to affect this ratio either. Our preliminary conclusion is that for NSs this ratio can be at least twice as large as the one coming from the BHs.

For all cases we compute the ejected material $M_{\text{esc}} = -\int \rho_0 u_t \sqrt{\gamma} d^3x$ for $r > 30M$ with specific energy $E > 0$ and positive radial velocity. We find that for cases NS1-Bh and ES1-Bh it is $\sim 0.2\%$ of the total rest-mass of the HMNS (see Fig. 3), and therefore it may give rise to an observable kilonova [59]. Also, the ejecta coming from HMNSs NS1, and ES1 are approximately three times larger than those coming from HMNSs NS2 and ES2. The reason for that is that NS1, ES1 have a larger density close to the surface than NS2 and ES2; therefore, when magnetic fields are present more mass in the outer layers can get ejected.

**Conclusions.**—We surveyed different HMNSs models with and without ergoregions with different initial strengths of the seeded magnetic field to probe the impact of ergoregions on launching magnetically−driven outflows. We found that magnetized HMNSs launch a mildly relativistic jet confined inside a tightly-wound-magnetic-field funnel whether or not an ergoregion is present. Our GRMHD simulations suggest that the properties of the outflow, such as maximum Lorentz factor ($\Gamma_L \sim 2.5$), the plasma parameter ($B^2/8\pi\rho_0 \lesssim 10$) and the magnetic collimation, are not affected by the ergoregion. Notice that, using force-free evolutions of magnetic fields on a fixed, homogeneous ergostar background and based on the similarities between the topology of the strongly force-free EM fields and the induced currents on the ergostar vs. the ones on a BH-disk, Ref. [35] concluded that the BZ mechanism is likely to operate in ergostars. As in [35] we do find some similarities in the topology of the magnetic fields (i.e. collimation) for our ergostar and BH spacetimes, although we find the same similarities when a magnetized normal HMNS, instead of an ergostar, is compared. The Poynting luminosity in the HMNS is comparable with that of the BH-disk remnant in which the BZ mechanism is operating, as well as with the luminosity reported by Ref. [38]. Hence the luminosity diagnostic cannot determine whether the BZ mechanism is operating or not. On the other hand the ratio $\Omega_F/\Omega_H$ turns out to be twice (at least) with the one computed in the BH-disk case. These results complement our previous studies with supramassive remnants [25] and suggest that in the hypermassive state it would be challenging for either normal stars or ergostars to be the origin of relativistic jets and the progenitors of sGRBs. Finally, we note here that similar maximum Lorentz factors and funnel magnetization have been reported in simulations that include neutrinos [30], so it is not clear if they can play a significant role in the formation of jets.

Although threading an ergostar with a magnetic field is by itself inadequate to launch a bona fide BZ jet, there remain mechanisms that can tap the rotational energy of the star by virtue of its ergoregion. These include the Penrose mechanism [60]. Noninteracting particles undergoing the Penrose process that can escape (e.g. various dark matter candidates) carry off energy and angular momentum. Particles that interact with the NS matter and are captured conserve (and redistribute) total angular momentum but can convert rotational kinetic energy into heat. Whether or not thermal emission from this heat may be detectable, the lifetime of the ergoregion and any emission, and the fate of the ergostar must all await further analysis.

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