Fast Ambiguous DOA Elimination Method of DOA Measurement for Hybrid Massive MIMO Receiver

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Abstract—DOA estimation for massive multiple-input multiple-output (MIMO) system can provide ultra-high-resolution angle estimation. However, due to the high computational complexity and cost of all digital MIMO systems, a hybrid analog digital (HAD) structure MIMO was proposed. In this paper, a fast ambiguous phase elimination method is proposed to solve the problem of direction-finding ambiguity caused by the HAD MIMO. Only two-data-blocks are used to realize DOA estimation. Simulation results show that the proposed method can greatly reduce the estimation delay with a slight performance loss.

Index Terms—Massive MIMO, DOA estimation, ambiguous phase elimination, hybrid analog digital structure

I. INTRODUCTION

Direction of Arrival (DOA) estimation has been widely used in many applications, including wireless communications, radar, navigation, sonar, tracking of various objects, secure and precise wireless transmission (SPWT), rescue and other emergency assistance equipment [1, 2]. In recent years, DOA estimation for massive multiple-input multiple-output (MIMO) system has attracted a lot of attention, which can provide super-resolution channel estimation and DOA estimation. However, as the number of antennas tends to large-scale, due to its high computational complexity and circuit cost, it is difficult for massive MIMO to be widely used in DOA measurement. To address this issue, in [3], a hybrid analog digital (HAD) structure MIMO was proposed, which can achieve similar or even lower the normalized mean square error (NMSE) with much less complexity compared to the maximum likelihood (ML) method. For a HAD MIMO system, the DOA measurement process falls into two stages: DOA estimation of generating a set of candidate solutions and cancelling spurious solutions. For a HAD MIMO, the major challenging problem is how to eliminate direction-finding ambiguity rapidly. A smart strategy of maximizing the average receive power was proposed to remove M − 1 spurious solutions in [3], where M is the number of antennas per subarray. This means it requires about M − 1 time slots to infer the true direction angle with each time slot being multiple snapshots or samples. This means a large processing delay of M time slots. In this paper, a fast ambiguous phase elimination method is proposed to find the true solution using only two-data-blocks by exploring the HAD structure with a slight performance loss.

II. SYSTEM MODEL

The HAD antenna array captures the narrowband signal s(t)ej2πfct from the θ0 direction emitted by a far-field transmitter, where s(t) is the baseband signal and fc is the carrier frequency. Here, a uniformly-spaced linear array (ULA) with N antennas is deployed and divided into K subarrays with each subarray containing M antennas where N = MK. Via analog beamforming (AB), radio frequency (RF) chains, analog-to-digital convertor (ADC) and digital beamforming (DB), the resulting receive signal is r(n) = vD HbA(θθ)(n) + w(n), where b denotes the index of time slots, each time slot consists of L snapshots, w(n) ∼ CN(0, σ2wI), and the AB matrix V A is a block diagonal matrix. Let us define ϕ = 2πd sin θ0, where λ represents the signal wavelength and d represents the antenna spacing.

III. CONVENTIONAL ROOT-MUSIC-HDAPA DOA ESTIMATOR

In the first stage, when all AB phases are zero, the output vector of sample n in time slot b is yAB(n) = M−1 aD(n)θθ(θθ) + wAB(n), where aD(n) = g(θθ)M(θθ), aM(n) = [1, e3iMϕ, ... , e3i(K−1)Mϕ]T, g(θθ) = M−1 M−1 m=1 e3i(m−1)ϕ. The set of candidate solutions to DOA is estimated by using the Root-MUSIC algorithm. The sample covariance matrix of the output vector of the antenna array is Ryy = 1/L M−1M−1 n=1 yAB(n)yABH(n), whose singular-value decomposition (SVD) is expressed as Ryy = [E S E N]E Mθθ EH[ E S E N]H, where E S and E N correspond to signal and noise subspaces, respectively. So the corresponding spectral function is PMU(θθ) = ||aMθθ(θθ)EH E N aD(θθ)||−1. Let us define the polynomial equation: fθ(θθ) = aH D(θθ)EH E N aD(θθ) ≜ f(z) ≜ fθ(ϕ) = 0, where z = e3iMϕ, and ϕ = Mϕ. The polynomial equation fθ(z) has 2K − 2 roots zi, which yields a set of associated emitter phases Θr = {ϕi, i ∈ {1, 2, ..., 2K − 2}}. Digital phase alignment (DPA) is used to delete 2K − 3 pseudo solutions in Θr and ϕr is obtained. Then we can get ϕr = 2πλ−1Md sin θθ. Since the function fθ(ϕ) is a periodic function of ϕ with period 2π, therefore, the extended feasible
solution set is \( \hat{\Theta} = \{ \hat{\theta}_i, i \in \{0, 1, \cdots, M-1\} \} \), where \( \hat{\theta}_i = \arcsin(\frac{\lambda(\hat{\theta}_i + 2\pi i)}{2\pi M}) \). Finally, analog phase alignment (APA) is used to eliminate the spurious solutions in the feasible set \( \hat{\Theta} \).

Considering the analog signal cannot be stored before ADC, the new \( M-1 \) time slots should be received to eliminate \( M-1 \) spurious direction ambiguity in \( \hat{\Theta} \). This will lead to a large estimation delay. To address this problem, a fast ambiguous subarray of group \( M \) is used to eliminate the spurious solutions in the new \( M \) ambiguous directions such that all phases of the subarray \( \{y_t(n)\} \) is as follows:

where \( H = (m-1)PM + (P-1)M \). The DB vector is set to be \( P_D = [1, 1, \cdots, 1]^T \). Therefore, the output signal through DPA is \( r_m(n) = \sum_{p=1}^{P} y_{mi}(n) \), and the average output power is

\[
P_r(\hat{\theta}_m) = \frac{1}{L} \sum_{n=1}^{L} [r_m(n) r_m(n)^H] = \frac{1}{L} \mathbf{r} \mathbf{r}^H
\]

where \( \mathbf{r} = [r(1), \cdots, r(L)] \). Eventually, the true direction angle corresponding to the maximum average power is

\[
\hat{\theta} = \arg \max_{\theta_m \in \Theta} P_r(\hat{\theta}_m)
\]

which completes the cancellation of spurious angles of requiring only one time slot. The delay is significantly reduced compared to the existing Root-MUSIC-HDAPA DOA Estimator method in \( [4] \). The ratio of their total time delays is \( 2/(M+1) \). As \( M \) increases, the rapid advantage of the proposed method over Root-MUSIC-HDAPA is more dramatic.

IV. PROPOSED FAST METHOD OF REMOVING SPURIOUS SOLUTIONS

Fig. 1 shows the basic idea of removing spurious directions with \( K \geq M \) in the second time slot. The total number \( K \) of subarrays is categorized into \( M \) groups of subarrays where each group has \( P = K/M \) subarrays. In this slot, the phases of receive APA are designed according to \( M \) ambiguous directions such that all phases of the subarray group corresponding to the true direction are aligned to output the maximum power after APA, the output signal of the \( p \)th subarray of group \( m \) is as follows:

\[
y_{mp}(n) = \mathbf{v}_{A,mp}^H \mathbf{a}_{mp}(\hat{\theta}_0) s(n) + w_{mp}(n) \tag{1}
\]

where

\[
\mathbf{v}_{A,mp} = \frac{1}{\sqrt{M}} [e^{j \alpha_{mp,0}}, e^{j \alpha_{mp,1}}, \cdots, e^{j \alpha_{mp,M-1}}]
\]

and

\[
\alpha_{mp,i} = \frac{2\pi}{\lambda} (H + i) d \sin \hat{\theta}_m \tag{3}
\]

where \( H = (m-1)PM + (P-1)M \). The DB vector is set to be \( P_D = [1, 1, \cdots, 1]^T \). Therefore, the output signal through DPA is \( r_m(n) = \sum_{p=1}^{P} y_{mi}(n) \), and the average output power is

\[
P_r(\hat{\theta}_m) = \frac{1}{L} \sum_{n=1}^{L} [r_m(n) r_m(n)^H] = \frac{1}{L} \mathbf{r} \mathbf{r}^H
\]

where \( \mathbf{r} = [r(1), \cdots, r(L)] \). Eventually, the true direction angle corresponding to the maximum average power is

\[
\hat{\theta} = \arg \max_{\theta_m \in \Theta} P_r(\hat{\theta}_m)
\]

V. COMPUTATIONAL COMPLEXITY ANALYSIS

The computational complexities of the existing method and proposed method are \( C_{\text{original}} = O(K^2L + (2(K-1))^3 + L(2K-2)K + N M) \), \( C_{\text{proposed}} = O(K^2L + (2(K-1))^3 + L((2K-2)K + N)) \) float-point operations (FLOPs). We can know that the computational complexity of the proposed method is reduced by \( M \) times when the ambiguous phase is eliminated.

VI. SIMULATION AND DISCUSSION

System parameters are chosen as follows: the direction of emitter \( \theta_0 = 41.345^\circ \), \( N = 64 \), \( M = 4 \), \( L = 8 \).

Table I illustrates the performances of root mean square error (RMSE) versus SNR of the proposed method and existing Root-MUSIC-HDAPA in \( [4] \). It can be seen from Table I that the proposed method is slightly worse than Root-MUSIC-HDAPA in terms of RMSE due to the use of far much less samples.

| SNR(dB) | -20 | -15 | -10 | -5 | 0 |
|--------|-----|-----|-----|----|---|
| RMSE(Proposed method) | 32.9 | 29.9 | 21.5 | 7.2 | 0.19 |
| RMSE(Root-MUSIC-HDAPA) | 29.3 | 25.3 | 18.4 | 5.7 | 0.18 |

Table II illustrates the performances of root mean square error (RMSE) versus SNR of the proposed method and existing Root-MUSIC-HDAPA in \( [4] \). It can be seen from Table II that the proposed method is slightly worse than Root-MUSIC-HDAPA in terms of RMSE due to the use of far much less samples.

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