Measurement of $ep \rightarrow e^\prime p\pi^+\pi^-$ and baryon resonance analysis

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Electromagnetic excitation of nucleon resonances is sensitive to the spin and spatial structure of the transition, which in turn is connected to fundamental properties of baryon structure, like spin-flavor symmetries, confinement, and effective degrees of freedom. In the mass region above 1.6 GeV, many overlapping baryon states are present, and some of them are not well known; measurement of the transition form factors of these states is important for our understanding of the internal dynamics of baryons. Many of these high-mass excited states tend to decouple from the single-meson channels and to decay predominantly into multi-pion channels, such as $\Delta$ or $Np$, leading to $N\pi\pi$ final states. Moreover, quark models with approximate (or “broken”) SU(6)$\otimes$O(3) symmetry predict more states than have been found experimentally; QCD mixing effects could decouple these unobserved states from the pion-nucleon channel while strongly coupling them to two-pion channels. These states would therefore not be observable in reactions with $\pi N$ in the initial or final state. Other models, with different symmetry properties and a reduced number of degrees of freedom, as e.g. in ref. 2, predict fewer states. Experimental searches for at least some of the “missing” states predicted by the symmetric quark models, which are not predicted by models using alternative symmetries, are crucial in discriminating between these models. Electromagnetic amplitudes for some missing states are predicted to be sizeable as well. Therefore, exclusive double-pion electroproduction is a fundamental tool in measuring poorly known states and possibly observing new ones.

In this paper we report a measurement of the $ep \rightarrow e'p\pi^+\pi^-$ reaction studied with the CEBAF Large Acceptance Spectrometer (CLAS) at Jefferson Lab. Beam currents of a few nA were delivered to Hall B on a liquid-hydrogen target, corresponding to luminosities up to $4 \times 10^{33}$ cm$^{-2}$s$^{-1}$. Data were taken in 1999 for about two months at beam energies of 2.6 and 4.2 GeV. Important features of the CLAS are its large kinematic coverage for multi-charged-particle final states and its good momentum resolution ($\Delta p/p \sim 1\%$). Using an inclusive electron trigger based on a coincidence between the forward electromagnetic shower calorimeter and the gas Cerenkov detector, many exclusive hadronic final states were measured simultaneously. Scattered electrons were identified through cuts on the calorimeter energy loss and the Cerenkov photo-electron distribution. Different channels were separated through particle identification using time-of-flight information and other kinematic cuts. We used the missing-mass technique, requiring detection in CLAS of at least $e\pi^+\pi^-$. The good resolution allowed selection of the exclusive final state, $ep\pi^+\pi^-$. After applying all cuts, our data sample included about $2 \times 10^5$ two-pion events.

The range of invariant hadronic center-of-mass (CM) energy $W$ (in 25 MeV bins) was 1.4-1.9 GeV for the first two bins in the invariant momentum transfer $Q^2$, 0.5-0.8 (GeV/c)$^2$ and 0.8-1.1 (GeV/c)$^2$, and 1.4-2.1 GeV for the highest $Q^2$ bin, 1.1-1.5 (GeV/c)$^2$. Data were corrected for acceptance, reconstruction efficiency, radiative effects, and empty target counts. They were further binned in the following set of hadronic CM variables: invariant mass of the $p\pi^+$ pair (10 bins), invariant mass of the $\pi^+\pi^-$ pair (10 bins), $\pi^-$ polar angle $\theta$ (10 bins), azimuthal angle $\phi$ (5 bins), and rotation freedom $\psi$ of the $p\pi^+$ pair with respect to the hadronic plane (5 bins). The full differential cross section is of the form:

$$
\frac{d\sigma}{dWdQ^2dM_{p\pi^+}dM_{\pi^+\pi^-}d\cos \theta_{\pi^-}d\phi_{\pi^-}d\psi_{p\pi^+}} = \Gamma_v \frac{d\sigma_v}{dWdQ^2dM_{p\pi^+}dM_{\pi^+\pi^-}d\cos \theta_{\pi^-}d\phi_{\pi^-}d\psi_{p\pi^+}}
$$

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\[
\Gamma_\nu = \frac{\alpha}{4\pi E^2 M_p^2} \frac{W(W^2 - M_p^2)}{(1 - \epsilon)Q^2}
\]

where \(\Gamma_\nu\) is the virtual photon flux, \(\frac{d\sigma}{d\tau}\) is the virtual photon cross section, \(\alpha\) is the fine structure constant, \(E\) is the electron beam energy, \(M_p\) is the proton mass, and \(\epsilon\) is the virtual photon transverse polarization. Systematic uncertainties were estimated as a function of \(W\) and \(Q^2\). The main sources were acceptance modeling, finite integration steps, and modeling of the radiative corrections, each one being at the 3 to 10% level. Each of the various cuts applied (fiducial, missing mass, etc.) contributed 2 to 5%. In Fig. 1 (left) we report the total virtual photon cross section as a function of \(W\) for all \(Q^2\) intervals analyzed. The CLAS data points clearly exhibit structures, not visible in previous data due to limited statistical accuracy.

Since existing theoretical models are limited to \(W < 1.6\) GeV, we have employed a phenomenological calculation for a first interpretation of the data. This model describes the reaction \(\gamma p \rightarrow p\pi^+\pi^-\) in the kinematic range of interest as a sum of amplitudes for \(\gamma p \rightarrow \Delta\pi \rightarrow p\pi^+\pi^-\) and \(\gamma p \rightarrow \rho \pi \rightarrow p\pi^+\pi^-\), while all other possible mechanisms are parameterized as phase space. A detailed treatment was developed for the non-resonant contributions to \(\Delta\pi\), while for \(\rho\pi\) production they were described through a simple diffraction ansatz. For the resonant part, a total of 12 states, classified as \(4^*\) decays, with sizeable \(\Delta\pi\) and \(\rho\pi\) decays, were included based on a Breit-Wigner ansatz. A few model parameters in non-resonant production were fitted to CLAS data at high \(W\), where the non-resonant part creates a forward peaking in the angular distributions, and kept fixed in the subsequent analysis. The phase between resonant and non-resonant \(\Delta\pi\) mechanisms was fitted to the CLAS data as well. To simplify the fits, we reduced eqn. (1) to three single-differential cross sections, \(\frac{d\sigma}{dM_{\pi^+\pi^-}}\), \(\frac{d\sigma}{dM_{\pi^+\pi^-}}\), and \(\frac{d\sigma}{d\cos\theta}\), by integrating over the other hadronic variables. These three 1-D distributions were then fitted simultaneously. Here \(\frac{d\sigma}{dM_{\pi^+\pi^-}}\) and \(\frac{d\sigma}{dM_{\pi^+\pi^-}}\) are both connected with the dominant \(\Delta^{++}\pi^-\) production reaction, while \(\frac{d\sigma}{d\cos\theta}\) is connected with \(p\rho\pi\) production. For each \(W\) and \(Q^2\) bin, a total of 26 data points from the three single-differential cross sections were used in our fits. The two edge points in both the \(p\pi^+\) and \(\pi^+\pi^-\) mass distributions were excluded as the model did not take into account the kinematic smearing in the \(M_{\pi^+\pi^-}\) versus \(M_{\pi^+\pi^-}\) plot caused by the \(W\) bin width.

The data analysis was performed in the following steps: (A) We produced reference curves using the available information on the \(N^*\) and \(\Delta\) resonances in 1.2-2 GeV mass range. Discrepancies between the CLAS data and our calculation were observed, which led to the subsequent steps B and C. (B) Data around \(W = 1.7\) GeV were fitted using the known resonances in the PDG but allowing the resonance parameters to vary in a number of ways. The best fit, corresponding to a prominent \(P_{13}\) partial wave, could be attributed to the PDG \(P_{13}(1720)\) resonance, but with parameters significantly modified from the PDG values. (C) As an alternative description, we introduced a new baryon state around 1.7 GeV. In what follows we describe each of the steps above in more detail.

Step (A) - To produce our reference curves, the \(Q^2\) evolution of the \(A_{1/2}\) and \(A_{3/2}\) electromagnetic couplings for the states was taken either from parameterizations of existing data, or from Single Quark Transition Model (SQTMs) fits where no data was available. For the \(P_{13}(1440)\) (Roper), given the scarce available data, the amplitude \(A_{1/2}\) was taken from a Non-Relativistic Quark Model (NRQM) fits. Partial \(LS\) decay widths were taken from a previous analysis of hadronic data and renormalized to the total widths from Ref. Results for step (A) are reported in Fig. (left). The strength of the \(D_{13}(1520)\) resonance at 1.5 GeV and the underlying continuum are well reproduced, except for the region on the low-mass side of the peak. However, a strong discrepancy is evident at \(W\) around 1.7 GeV. Moreover, at this energy the reference curve exhibits a strong peak in the \(\pi^+\pi^-\) invariant mass (Fig. (right)), connected to sizeable \(\rho\pi\) meson production. This contribution was traced back to the 70-85% branching ratio of the \(P_{13}(1720)\) into this channel.

Step (B) - Starting from the above mentioned reference values, the parameters of various states were varied in order to fit the CLAS data. In this discussion, we restrict ourselves to the discrepancy around 1.7 GeV and the few
TABLE I: PDG $P_{13}(1720)$ parameters from fit (B) and new state parameters from fit (C). Errors are statistical.

|          | M (MeV) | $\Gamma$ (MeV) | $\frac{d\sigma}{dM}$ (%) | $\frac{d\sigma}{d\cos\theta}$ (%) |
|----------|---------|----------------|--------------------------|-----------------------------------|
| PDG $P_{13}$ (B) | 1725±10 | 114±19         | 63±12                    | 19±9                             |
| PDG [1]   | 1650-1750 | 100-200       | N/A                      | 70-85                            |
| new $P_{13}$ (C) | 1720±20 | 88±17          | 41±13                    | 17±10                            |

resonant states relevant in this energy region. All fit $\chi^2/\nu$ values were calculated from the 8 W bins between 1.64 and 1.81 GeV and from the 3 $Q^2$ bins (624 data points). The number of free parameters ranged from 11 to 32, depending on the fit, corresponding to $\nu=613$ to 592 degrees of freedom. Assuming the resonance properties given by the PDG, the bump at about $W=1.7$ GeV cannot be due to the $D_{13}(1675)$, $F_{15}(1680)$, or $D_{33}(1700)$ states; the first because its well known position cannot match the peak; the second because of its well known position and photocouplings [4]; the third due to its large width ($\sim$300 MeV). The remaining possibilities from the PDG are the $D_{13}(1700)$, the $P_{13}(1720)$, and the $P_{11}(1710)$ (the latter not present in step (A)), for which no data on $A_{1/2}$ or $A_{3/2}$ at $Q^2 > 0$ are available [4]. If no configuration mixing occurs, the $D_{13}(1700)$ cannot be excited in the SQTM, while the SQTM prediction for the $P_{13}(1720)$ relies on ad hoc assumptions. According to the literature [1, 4, 3], hadronic couplings of the $D_{13}(1700)$ and the total width of the $P_{13}(1710)$ are poorly known, while the $P_{13}(1720)$ hadronic parameters should be better established. Several other partial waves were investigated in step (C).

To improve our reference curves before fitting the bump at around 1.7 GeV, the following steps were carried out: the $P_{11}(1440)$ strength was fitted to our low W data; the $D_{15}(1675)$ and the $D_{13}(1700)$ photocouplings (which vanish in the SQTM) were replaced by NRQM values from Ref. [3]; an empirically established $A_{1/2,3/2}$ SQTM fitting uncertainty or NRQM uncertainty of 10 or 20% ($\sigma$) was applied to all $N^*$ states; the hadronic parameters were allowed to vary for the $D_{13}(1700)$ according to Ref. [4], and finally, the curves providing the best $\chi^2/\nu$ were selected as the starting points. Then, first we performed three fits, (B1), (B2), and (B3), where the photocouplings of only one resonance at a time were varied. In (B1), we varied $A_{1/2}$, $A_{3/2}$, hadronic couplings, and position of the $D_{13}(1700)$ in a wide range. In (B2), the same was done for the $P_{13}(1720)$, and in (B3) for the $P_{11}(1710)$. In both fits (B2) and (B3), we also varied the hadronic parameters and the position of the $D_{13}(1700)$ over a range consistent with their large uncertainties from Ref. [4]. Fits (B1) and (B3) gave a poor description of the data, with $\chi^2/\nu$=5.2 and 4.3, respectively. The best fit ($\chi^2/\nu$ =3.4) was obtained in (B2) (Fig. 2). However, the resulting values for the branching fractions of the $P_{13}(1720)$ were significantly different from previous analyses reported in the literature and well outside the reported errors [1, 3, 4]. Starting from (B3), we then performed a final fit, (B4), for which the $P_{13}(1720)$ hadronic couplings were fixed from the literature, and varying the photocouplings of all three candidate states, $D_{13}(1700)$, $P_{13}(1720)$, and $P_{11}(1710)$, by 100% ($\sigma$). No better solution was found, the $\chi^2/\nu$ being 4.3 (Fig. 2). In Fig. 3, we report the final comparison of fits (B2) and (B4) with the total cross section data. Table I shows our results (first row) with statistical uncertainties, in comparison with the PDG values (second row). Our fits were not providing an unambiguous separation of $A_{1/2}$, $A_{3/2}$, and the longitudinal $S_{1/2}$, so we report as result the total photodisintegration cross section for $\gamma p \rightarrow p\pi^+\pi^-$ as a function of $W$ from CLAS at the 3 mentioned $Q^2$ intervals (see fig.1). The error bars are statistical only. The curves (see text) correspond to the fits (B2) (red), and (B4) (blue). Right: subdivision of the fitted cross section (B2) for $Q^2$=0.5-0.8 (GeV/c)^2 into resonant $\Delta^{++}\pi^-$ (black solid), continuum $\Delta^{++}\pi^-$ (black dashed), resonant $\rho^0p$ (magenta solid), and continuum $\rho^0p$ (magenta dashed). Notice the different vertical scales.

FIG. 3: Left: Total cross section for $\gamma p \rightarrow p\pi^+\pi^-$ as a function of $W$ from CLAS at the 3 mentioned $Q^2$ intervals (see fig.1). The error bars are statistical only. The curves (see text) correspond to the fits (B2) (red), and (B4) (blue). Right: subdivision of the fitted cross section (B2) for $Q^2$=0.5-0.8 (GeV/c)^2 into resonant $\Delta^{++}\pi^-$ (black solid), continuum $\Delta^{++}\pi^-$ (black dashed), resonant $\rho^0p$ (magenta solid), and continuum $\rho^0p$ (magenta dashed). Notice the different vertical scales.
The quantum numbers $S$, $I$, and $P$ determine the hadronic parameters of the excited electromagnetically. This possibility is studied in previous analyses may have much larger uncertainties than reported in the literature. In this case, outlined in our step (B), our analysis would establish new, more precise parameters for a known state, and invalidate previous results.

In conclusion, in this letter we presented data on the $ep \rightarrow e'p\pi^+\pi^-$ reaction in a wide kinematic range, with higher quality than any previous double pion production experiment. Our phenomenological calculations using existing PDG parameters provided a poor agreement with the new data at $W \sim 1700$ MeV. We explored two alternative interpretations of the data. If we dismiss previously established hadronic parameters for the $P_{13}(1720)$ we can fit the data with a state having the same spin/parity/isospin but strongly different hadronic couplings from the PDG state. If, alternatively, we introduce a new state in addition to the PDG state with about the same mass, spin, and positive parity, a good fit is obtained for a state having a rather narrow width, a strong $\Delta\pi$ coupling, and a small $pN$ coupling, while keeping the PDG $P_{13}(1720)$ hadronic parameters at published values. In either case we determined the total photocoupling at $Q^2 > 0$. A simultaneous analysis of single and double-pion processes provides more constraints and may help discriminate better between alternative interpretations of the observed resonance structure in the CLAS data. Such an effort is currently underway.

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