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Soliton-radiation trapping in gas-filled photonic crystal fibers

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We propose an optical trapping technique in which a fundamental soliton traps an ultrashort small amplitude radiation in a symmetric hollow-core photonic crystal fiber filled with a noble gas, preventing its dispersion. The system is Raman- and plasma-free. Trapping is due to the cross phase modulation effect between the two pulses. The trapped radiation inside the soliton-induced potential will oscillate periodically due to the shock effect, similar to the motion of a mechanical pendulum.

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I. INTRODUCTION

Optical trapping has been predicted and demonstrated in a variety of different situations since the invention of low-loss optical fibers [1]. Self-trapping is at the core of the existence of optical solitons, where the nonlinear self-phase modulation (SPM) is used to compensate the group velocity dispersion [2]. Bright and dark solitons have been observed in the anomalous and the normal dispersion regimes, respectively, in a number of elegant experiments [3–5]. Hasegawa has suggested the nonlinear cross-phase modulation (XPM) effect as a fundamental trapping mechanism between different pulses, when their group velocities are matched [6]. Via XPM and by utilizing the waveguide dispersion to compensate for the group velocity mismatch, the possibility of forming ultrashort pulses of stimulated Raman radiation has been predicted [7]. Trapping can also naturally occur between a pair of pulses lying in opposite dispersion regimes, since the group velocity matching condition is easily satisfied by frequency detuning. For instance, redshifted solitons due to intrapulse Raman scattering can trap across the zero dispersion wavelength weak blueshifted dispersive wave packets on the femtosecond scale [8–14]. In an unconventional situation, a bright soliton can also be trapped in the normal dispersion, when it is coupled to a dark soliton in the anomalous dispersion regime [15–17]. Moreover, a bright soliton can propagate stably in the normal dispersion regime with the aid of a soliton-pair copropagating in the anomalous dispersion regime [18,19].

The invention of photonic crystal fibers (PCFs) is a milestone in the field of nonlinear fiber optics [20,21]. Hollow-core (HC) PCFs have been exploited to explore the nonlinear interaction of light in a new wide range of distinct media. HC-PCFs based on a kagome lattice have been successfully used recently in the investigation of light-matter interactions in the presence of gases [22]. Filling these fibers by a Raman-active gas, a drastic reduction in Raman threshold has been obtained [23]. High harmonic, and efficient deep UV generation have been also demonstrated in HC-PCFs filled by noble (Raman-inactive) gases [24,25]. Using intense broadband pulses to access the ionization regime of the noble gases, soliton self-frequency blueshift has been observed and thoroughly studied in these fibers [26–29]. On the other hand, launching intense narrow-band pulses can lead to ionization-induced asymmetric SPM and universal modulational instability [30].

In this paper, we show that optical trapping between two different short pulses can exist, when both pulses propagate together in the anomalous dispersion regime of a HC-PCF filled by a noble gas. The intensities of the two pulses are below the ionization limit of the gas.

II. PRINCIPLE OF OPERATION AND SYSTEM DESIGN

Consider the propagation of two short pulses in a guided nonlinear-Kerr medium. We assume that only one of the two pulses is intense enough to induce nonlinear phenomena, and that the dispersion is anomalous for both pulses. Hence, the strong pulse can maintain its temporal shape due to the induced SPM, while the other pulse will suffer from strong dispersion due to the absence of compensation between nonlinear and dispersive effects. Only if the two pulses can propagate with the same group velocity, the nonlinearity of the strong pulse will affect the second pulse via XPM that can compensate the dispersion-induced broadening, and the weak pulse will propagate as a temporally localized radiation. In analogy with quantum mechanics, the strong pulse creates a potential well that traps the weak pulse inside it, and both pulses travel together without suffering from dispersion-induced broadening [13,14,18,19]. If the nonlinear medium is Raman- or plasma-free, the dispersion must be anomalous for both pulses to allow dispersion compensation to take place.

To observe this temporal trapping due to the soliton-induced potential, we require a nonlinear-Kerr medium, where two different ultrashort pulses lying in the same anomalous dispersion regime can acquire a common group velocity. In previous works, the group velocity matching condition was achieved when a redshifting soliton was in the anomalous dispersion and a small amplitude wave was in the normal dispersion regime [13,14]. One possible technique for our proposal is to use a solid-core PCF with multiple zero dispersion wavelengths. However, this type of fiber requires high fabrication tolerance. Moreover, undesirable emission of resonant radiation will be out of control in these fibers. Another technique is to launch the two pulses in two different polarization states in an elliptical solid-core fiber. In order to minimize the Raman effect in both techniques, relatively long pulses that suffer from insignificant dispersion-induced broadening must be used. Hence, the attracting feature of trapping ultrashort pulses will be lost.
A HC-PCF filled by a noble (Raman-inactive) gas and with a symmetric core is considered to be the perfect host to demonstrate our proposal. This can be achieved by launching two different pulses with the same frequency, however, in two different circular polarization states, in the deep anomalous dispersion regime of the fiber. Having the same frequency allows the two pulses to have the same group velocity, as well as to be naturally in the same dispersion regime. Using different polarization states allows one to separate the two pulses at the fiber output. The reason for using circular polarization states is to avoid unwanted additional nonlinear phenomena that can emerge if linearly polarized states are injected [2].

III. GOVERNING EQUATIONS FOR SOLITON-RADIATION TRAPPING

To study the induced trapping between a propagating strong pulse and a small amplitude radiation with the same central frequency, we consider the linearly polarized states injected [2]. This can be achieved by launching two different pulses with the same frequency, however, in two different circular polarization states, in the dispersion regime of the fiber. Having the same frequency allows the two pulses to have the same group velocity, as well as to be naturally in the same dispersion regime. Using different polarization states allows one to separate the two pulses at the fiber output. The reason for using circular polarization states is to avoid unwanted additional nonlinear phenomena that can emerge if linearly polarized states are injected [2].

![Image](https://example.com/image.png)

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IV. SHOCK EFFECT

Since the nonlinear medium is Raman- and plasma-free, and the two pulses are supposed to be arbitrarily short, the self-steeping (shock effect) will have a significant role in the pulse dynamics. In this case, Eq. (2) becomes

\[
\begin{align*}
&i\hat{\partial}_t \psi_1 + \frac{1}{2} \hat{\partial}_x^2 \psi_1 + |\psi_1|^2 \psi_1 = -i r_{\text{sh}} \partial_t (|\psi_1|^2 \psi_1), \\
&i\hat{\partial}_t \psi_2 + \frac{1}{2} \hat{\partial}_x^2 \psi_2 + 2|\psi_1|^2 \psi_2 = -2 r_{\text{sh}} \partial_t (|\psi_1|^2 \psi_2),
\end{align*}
\]

where \( r_{\text{sh}} \equiv (\omega_0 t_0)^{-1} \) is the normalized shock coefficient, and \( \omega_0 \) is the input pulse central frequency. In order to study the shock effect on both the soliton and the radiation, we will adapt the variational perturbation method for our problem [2]. Using this method, the right-hand sides of the above coupled equations are considered as perturbations for the previously obtained solutions of \( \psi_1 \) and \( \psi_2 \). Hence, the soliton and the radiation will maintain their functional shape during propagation, however, their parameters will vary. For both pulses, one has to obtain the Lagrangian \( \mathcal{L} = \int_{-\infty}^{\infty} L_\psi \, dt \), where \( L_\psi \) is the Lagrangian density. Using the reduced Euler-Lagrange equations, a set of ordinary differential equations that tracks the spatial evolution of the pulse parameters can be obtained. Since this technique is well illustrated in the literature...
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FIG. 1. (Color online) (a), (b) Propagation of a dispersive radiation solely in an argon-filled HC-PCF, when the radiation takes the form of (a) the fundamental mode \( f_0(\tau) \), or (b) the first-order mode \( f_1(\tau) \). (c)–(h) Propagation of a fundamental soliton and a dispersive radiation together in an argon-filled HC-PCF. The group-velocity matching condition is satisfied. The two pulses have the same central wavelength \( \lambda = 800 \text{ nm} \), and opposite circular polarizations. (c), (d) Temporal and spectral evolution of the soliton. (e)–(h) Temporal and spectral evolution of the radiation, when it is in the fundamental mode [(c), (f)], or in the first-order mode [(g), (h)]. Other simulation parameters are \( \eta = 8.9 \), \( \psi_0 = 0.5 \), and \( \tau_0 = 50 \text{ fs} \). The higher-order dispersion and self-steepening effects are neglected.

FIG. 2. (Color online) Propagation of a fundamental soliton and a dispersive radiation in an argon-filled HC-PCF in the presence of the self-steepening effect. Other simulation parameters are similar to those used in Fig. 1. Temporal and spectral evolution of the radiation, when it is in the fundamental mode [(a), (b)], or in the first-order mode [(c), (d)], respectively. Solid black lines are the numerical solutions of the coupled differential equations (7).

where \( I = \sqrt{\pi} \Gamma(p_0)/\Gamma(p_0 + \frac{1}{2}) \), \( g(\tau) = p_0 \tanh[a(\tau - \tau_p)] \), \( \Gamma \) is the gamma function, and \( \text{Re} \) stands for the real part. These coupled equations can be solved numerically.

The effect of the shock term on the radiation is depicted in Fig. 2, which shows the temporal and the spectral evolution of the dispersive radiation. As shown in panel (a), the radiation acquires a varying group velocity, which differs from that of the soliton. The reason is related to the factor 2 that distinguishes between the SPM and XPM processes [see Eq. (4)]. This group velocity difference between the two pulses causes the observed periodic oscillations of the radiation inside the soliton-induced potential. The dynamics of the radiation is similar to the motion of a mechanical pendulum, or an oscillating particle inside a potential. Initially, the particle is settled at the potential minimum. Due to the shock effect, it acquires a velocity that is highest in correspondence with that minimum. As the “particle” (which is in our case the small amplitude radiation) moves upward, it undergoes a deceleration, resulting in a spectral blueshift as shown in panel (b). When the particle reaches its maximum position, it stops and changes its direction downwards, acquiring an acceleration that corresponds to a spectral redshift. Passing by the potential minimum, the particle goes upward to the other side of the potential. This periodic motion continues during the propagation along the fiber. In the case of the fundamental mode, there is a good qualitative agreement between the analytical and numerical results [see Figs. 2(a) and 2(b)]. The odd mode behaves similarly to the even mode as portrayed in panels (c) and (d). However, the analytical results fail to mimic the numerical ones in this case. We attribute this to the fact that the radiation does not preserve its temporal shape during

\[
 \frac{d\delta}{d\xi} = -2\eta^2 \frac{1}{\psi_0^2} \int_0^\infty g(t)(\text{Im}[\psi_0^2] + 2|\psi_1|^2|\psi_2|^2)dt, \\
 \frac{d\tau_p}{d\xi} = -\delta + 2\eta \frac{1}{\psi_0^2} \int_0^\infty \text{Re}(\tau - \tau_p)e\psi_0^2 dt, \\
\]

\[
\psi_0^2 &= \frac{\epsilon}{2} |\psi_1|^2 + \frac{\eta^2}{2} \left| \frac{\partial}{\partial \xi} \psi_1 \right|^2, \\
I &= \sqrt{\pi} \Gamma(p_0)/\Gamma(p_0 + \frac{1}{2}), \quad g(\tau) = p_0 \tanh[a(\tau - \tau_p)].
\]

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propagation. The two lobes that constitute the radiation packet exchange energy, similar to partial coupling between adjacent waveguides, and this prevents the perturbation theory from being a good approximation of the dynamics.

V. CONCLUSIONS

We present a trapping technique between a strong fundamental soliton and a weak dispersive radiation in a symmetric HC-PCF filled by a noble gas. The medium is Raman- and plasma-free. Trapping is due to the cross-phase modulation effect between the two pulses having the same central frequency being a good approximation of the dynamics. From a quantum mechanics point of view, the soliton creates a potential well that traps the particlelike radiation inside, and the two pulses travel together without suffering dispersion-induced broadening. This potential well allows for only two bound states. Exact analytical formulas for the fundamental and the first-order modes of the radiation have been obtained. The soliton shock effect leads to a periodic oscillation of the radiation inside the potential, similar to a pendulum motion. As a consequence, the radiation central frequency is shifted periodically.

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