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Published in: Journal of Physics: Conference Series (Online)

Link to article, DOI: 10.1088/1742-6596/753/2/022050

Publication date: 2016

Document Version
Publisher's PDF, also known as Version of record

Citation (APA):
Rogowski, K., Hansen, M. O. L., Maronski, R., & Lichota, P. (2016). Scale Adaptive Simulation Model for the Darrieus Wind Turbine. Journal of Physics: Conference Series (Online), 753, [022050]. https://doi.org/10.1088/1742-6596/753/2/022050
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Scale Adaptive Simulation Model for the Darrieus Wind Turbine

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Abstract. Accurate prediction of aerodynamic loads for the Darrieus wind turbine using more or less complex aerodynamic models is still a challenge. One of the problems is the small amount of experimental data available to validate the numerical codes. The major objective of the present study is to examine the scale adaptive simulation (SAS) approach for performance analysis of a one-bladed Darrieus wind turbine working at a tip speed ratio of 5 and at a blade Reynolds number of 40,000. The three-dimensional incompressible unsteady Navier-Stokes equations are used. Numerical results of aerodynamic loads and wake velocity profiles behind the rotor are compared with experimental data taken from literature. The level of agreement between CFD and experimental results is reasonable.

1. Introduction

According to the EWEA report “Wind in power: 2015 European statistics – February 2016”, wind energy has become very popular in the EU and around the world. Research shows that not only large wind farms are profitable, some economic studies show profitability of small wind turbines in specific geographical areas e.g. for Iran [1], the Hawaiian Islands [2], Egypt [3] etc. An economic analysis of the installation and use of small wind turbines for five major EU countries were made by Bortolini et al. with positive results [4].

Small-scale wind turbines can use a horizontal axis as well as a vertical axis concept. Vertical-axis wind turbine (VAWT) with the Darrieus concept is lift force driven and is an alternative to the horizontal axis wind turbine (HAWT) [5]. The Darrieus wind turbine consists of two or more curved blades, however, straight-bladed rotors or rotors with twisted blades are more common in applications for small wind turbines [6]. VAWT can operate, by design, independently of wind direction and therefore a yaw control system is not required. The motivation for the research of small-scale vertical-axis wind turbine is a demand for decentralized electricity generation in urban and rural areas [7].

In the case of vertical axis wind turbines, flow around the rotor blades is very complex. During the rotation many phenomena can occur, such as for example: dynamic deep stall, wake-blade-wake interaction, secondary effects of tower, struts, blade shape and aspect ratio [8]. The use of rotor consisting of a single blade seems to be a good idea to understand the basis of principles of operation...
of the wind turbine. Knowing the nature of fluid flow for a one-bladed rotor it is possible to optimize the rotor configuration (e.g. the number of blades and their airfoil) to maximize the power production.

Experimental measurements of aerodynamic loads is a very difficult task because the flow around the rotor is unsteady, and therefore only two experiments of one-bladed rotor were carried out at the turn of the 70s and 80s [9] and [10]. Strickland et al. [9] measured aerodynamic loads also for different rotor configurations and for different operating conditions. Aerodynamic blade loads for straight-bladed rotor consisting of two blades and tower were performed by Laneville and Vittecoq [11]. Ferreira et al. [12] have shown that it is possible, though crudely, that blade loading can be extracted from velocity flow fields using a method that they have developed.

Nowadays computational fluid dynamics (CFD) is a significant tool modelling wind turbines aerodynamics. Numerical investigation of the two-dimensional unsteady flow around a NACA 0015 airfoil for a Darrieus type wind turbine under dynamic stall conditions are performed by Allet et al. [13]. Authors used the non-equilibrium Johnson-King model and the algebraic Cebeci-Smith turbulence model. CFD simulations of the one-bladed rotor, using the $k$-$\varepsilon$ turbulence model, was also made by Hansen and Sørensen [14]. The 15kW small-scale VAWT developed by Edinburgh Designs Ltd. was examined numerically using the SST $k$-$\omega$ turbulence model by Gretton et al. [15]. A CFD method with the same turbulence model was used by Marsh et al. [16] to simulate a small-scale straight-bladed VAWT operating in water. The obtained results of Marsh et al. for the power coefficient of 3D VAWTs were comparable with a simplified aerodynamic model – the double multiple stream model.

The scale-adaptive simulation (SAS) is a relatively new approach in modelling unsteady turbulent flows. The formulation of this two-equation model can operate in RANS mode [17]. However, the SAS model can resolve unsteady turbulent structures adapting the length-scale automatically to the resolved scales of the flow field [18]. One of the main advantages of this model is that it is able to obtain results similar to the DES turbulence model reducing the cost of computing [17].

A one-bladed vertical-axis wind turbine with the Darrieus rotor is not used in the industry. However, the use of such the turbine for research is justified because the analysis of the flow past its rotor is easier. The main objective of the present research is the analysis of aerodynamic blade loads and aerodynamic wake of a one-bladed Darrieus-type rotor based on the experiment of Strickland at al. [9]. Four main questions have been addressed:

(i) What are the differences in aerodynamic loads for different turbulence models?
(ii) What are the differences in the velocity field computed using different turbulence models?
(iii) How the rotor blade interacts with the aerodynamic wake?
(iv) What are the differences in vorticity field for classical turbulence model and the SAS model?

2. Blade loads and aerodynamic wake

In order to explain the principle of operation of the Darrieus wind turbine, the turbine rotor has been cut with a plane perpendicular to its axis of rotation. Analysing the velocity triangle near a blade the lift and drag loads can be computed for various azimuthal positions (Figure 1). The aerodynamic loads can be projected to the chordwise and the radial directions yielding the normal and tangential loads, $F_N$ and $F_T$, respectively. Most often they are given as dimensionless coefficients:

$$CF_N = \frac{F_N}{0.5\rho V_0^2 c}$$  \hspace{1cm} (1)

$$CF_T = \frac{F_T}{0.5\rho V_0^2 c}$$  \hspace{1cm} (2)

where: $\rho$ is the medium density, $V_0$ is the wind speed and $c$ is the chord length. Aerodynamic loads depend on rotor position defined by azimuth $\theta$. The aerodynamic forces shown in the article are
presented as functions of the azimuth angle where the initial position and the direction of the azimuth have been adopted as in Figure 1.

The wake characteristics are evaluated at a distance of one rotor diameter behind the rotor to be consistent with measurements. Figure 1 shows also the airfoil path and location of checkpoints for velocity measurement behind the rotor.

![Figure 1. Velocity vectors, forces, angles and checkpoints for wake velocity computations.](image)

3. Experimental data
The results from Strickland’s water channel experiments [9] at Texas Tech University are used to validate the numerical model. A series of two-dimensional experiments were conducted in a water towing tank for rotors with different number of straight blades operated at different conditions. The rotor was mounted on a special carriage which could slide along a fixed rail. By selection of appropriate towing speed and rotational velocity of the rotor the blade Reynolds number of 40 000 was ensured. The use of water as a working fluid allowed easier measurement of aerodynamic blade forces as functions of time and easier flow visualization around the rotor. One of the main objectives of the experiments was to measure the aerodynamic blade loads and velocity profiles behind the rotor. Aerodynamic blade loads were measured by strain gages. The signal generated by the Wheatstone bridge was amplified and sent via slip rings to an eight channel recorder and oscilloscope [9]. Velocity profiles were measured by velocity transducer placed behind the rotor. Measures were repeated many times for thirteen check points at various spanwise locations as depicted in Figure 1. Due to limited space in this article the description of the experiment is very short and more information can be found in the report [9].

In this paper validation of numerical results is done using the experimental results taken from [9] for a one-bladed rotor operating at a tip speed ratio of 5.

4. CFD model of the Darrieus rotor
4.1. Rotor configuration and operating conditions
Numerical analyses of the 2D VAWT are performed for the same conditions as in the experiment [9]. A straight-bladed rotor using one blade only with a NACA 0012 airfoil and a diameter of 1.22m
rotating at an angular velocity of 0.75 rad/sec is simulated. This corresponds to a blade Reynolds number of 40,000 and a tip speed ratio of 5 for an undisturbed water velocity of 0.091 m/sec. The solidity of the rotor, defined as a ratio of the airfoil chord to the rotor radius, is 0.15 for the chord of 0.0914 m.

4.2. CFD model
In this study an unsteady viscous flow around the basically 2D geometry of the wind turbine has been considered and the sliding mesh model has been used. Although, the geometry is 2-D the rotor computations are done in 3-D. The computational domain is three-dimensional and its thickness is equal to two airfoil chords. Figure 2 presents the CFD model. The idea behind the solution of such 2D/3D problem is a better representation of the turbulent flow that is by nature 3-D and unsteady. The sliding mesh model requires defining the domains that move relative to the others. Therefore, the computational domain used during the simulations consists of two independently meshed cell zones: a large stationary square zone with a length of \(a\) and a smaller rotating circle zone around the rotor with a radius of \(R_i\). These zones are meshed independently and they are bounded by a grid interface. It was argued that the size of the square domain \(a\) should be minimum 10 times larger than the rotor diameter \([19]\) and \([20]\). Therefore the size \(a\) is taken to be 12D, where D is the rotor diameter. It has been assumed that the radius \(R_i\) is equal to 1.5R, where R is a rotor radius.

![Figure 2. CFD model of the Darrieus wind turbine.](image1)

![Figure 3. 3D CFD mesh around the blade.](image2)

The three-dimensional mesh is comprised by hexahedral elements. Distribution of the 3D mesh in a plane perpendicular to the axis of rotation of the Darrieus type wind turbine is the same as for a two-dimensional mesh. The 2D mesh consists of structured mesh with quadrilateral elements near the profile edges and unstructured mesh, also with quadrilateral elements, elsewhere. Mesh analysis of 3D mesh has been performed in two steps. First, the Darrieus type rotor performance has been examined for 2D mesh. Secondly, the results from the rotor 3D mesh are compared with results from the 2D mesh. Figures 2 and 3 present the 3D computational domain and the mesh for 2D CFD model, respectively.

Mesh sensitivity analysis of the 2D mesh has been performed for different parameters such as, for example: the length of the finite element mesh on a profile edge (edge sizing), growth rate of structured mesh in the boundary layer, growth rate of unstructured mesh and the number of layers of structured mesh. During the study it is found that the distribution of the structural grid has the greatest impact on the results of aerodynamic loads. Figure 4 shows the tangential force coefficient as a function of azimuth position computed using the SAS turbulence model for three values of edge sizing 0.0001 m; 0.00025 m and 0.0004 m. As it can be seen from this figure the differences in the computed tangential force are very small for the three different length in the computational grid. Due to limited
space in the paper, only the effect of one parameter of the mesh on the aerodynamic loads is shown graphically. The final grid has the following parameters: the edge sizing is 0.0025, the number of layers of structured mesh is 50, growth rate of structured mesh is 1.1 and growth rate of unstructured mesh is 1.04. 3D mesh has been created on the basis of the 2D grid by extending it along the span. The number of elements of the mesh along the span of the blade is 30. The final 3D mesh consist of 3 958 740 elements.

\[ \text{Figure 4. The tangential force coefficient vs. azimuth position for the SAS model and for three values of edge sizing.} \]

4.3. Turbulence modelling

The performance of the Darrieus wind turbine is computed using the unsteady Reynolds-averaged Navier-Stokes (URANS) turbulence schemes. The authors used the relatively recent turbulence model, scale adaptive simulation (SAS), for the simulation of flow around the rotor. The transient and 3-D results obtained using this model are compared with the more popular the RNG k-\( \varepsilon \) turbulence model as well as the SST k-\( \omega \) turbulence model which is popular in VAWT applications. The value of turbulence intensity is assumed very low and equal to 0.1%.

The SAS is an improved URANS turbulence model developed by Menter for the simulation of unsteady turbulent flows. For stable flow regions the SAS can operate as a standard RANS model. Classical URANS models produce only the large-scale unsteadiness in unstable flow conditions, whereas, the SAS concept adapts the turbulence length-scale automatically to the resolved scales of the flow field. In other words, the SAS model provides URANS with “LES”-content in unsteady regions [17]. The formulation of the SAS model is based on two transport equations from the SST k-\( \omega \) model. However, the transport equation for the turbulence eddy frequency \( \omega \) in the SST k-\( \omega \) model is modified by additional source term derives from a second order derivative term in Rotta’s transport equations. The SAS concept uses the von Karman length-scale into the turbulence scale equation. Contrary to the detached eddy simulation (DES) model, the SAS model has fewer requirements for the mesh distribution in unsteady regions because DES provides LES-behaviour via explicit grid influence. The detailed derivation can be found in the ANSYS Help Version 15.0.0.
5. Results

5.1. Aerodynamic loads

Results of aerodynamic loads, tangential and normal components, are depicted in Figures 5 and 6. The numerical results for the SAS 2D, the SAS 3D, the SST $k-\omega$ 2D and the RNG $k-\varepsilon$ 3D turbulence models are compared with the experimental results of Strickland et al. [9]. Due to limits on the computational time on a supercomputer, the results for the SST $k-\omega$ turbulence model are presented here for the 2D model of vertical-axis wind turbine. Figure 5 presents the comparison of the tangential force obtained for the 2D mesh and 3D mesh having the same mesh distribution in the plane perpendicular to the axis of rotation. As it can be seen from the figure, the three-dimensional mesh gives results almost the same as the two-dimensional grid. The CFD results of the tangential force are significantly different for the azimuth 90-170 degrees. This is caused by flow characteristics (flow velocity distribution and pressure distribution) that are different for the RNG $k-\varepsilon$ model and for the following models: the 2D SAS, the 3D SAS and the SST $k-\omega$. The tangential force computed using the SAS models and the SST $k-\omega$ model are lower than the experimental one in the range of azimuths between 90 and 170deg whereas the RNG $k-\varepsilon$ model overestimates the results of this force component. As a result, the power coefficient computed by the SAS models and by the SST $k-\omega$ is about 0.08-0.1 whereas by the RNG $k-\varepsilon$ model is about 0.25. Moreover, it should be emphasized that, in the case of the SAS models as well as the SST $k-\omega$ model, the results of the tangential blade loads seems to be better for the leeward side of the rotor in comparison with the RNG $k-\varepsilon$ model. The results of the normal force computed by CFD are in reasonable agreement with the experimental results. The SAS model predicts a local extreme of the tangential load at the azimuth of 135 deg. This kink is not presented by other turbulence models and by the experiment. This is because, contrary to the RNG $k-\varepsilon$ and the SST $k-\omega$ models, the SAS shows unsteadiness near the leading edge of the blades and evolves in the next sequences of fluid motion. Accuracy of measuring instruments used in the experiment may be insufficient to capture the small changes in aerodynamic loads. In order to explain the differences in the results of aerodynamic loads at the range of azimuth position between 90 and 170 degrees, the analysis of the static pressure and the vorticity is presented in the next subsections.

![Figure 5. Non-dimensional tangential aerodynamic blade force.](image-url)
5.2. Static pressure distribution and vorticity

In some ranges of azimuth all examined turbulence models give similar results for the aerodynamic loads. Therefore, in these ranges of azimuth, pressure distribution computed using these turbulence models should also be similar. Figures 7 and 9 show the distribution of static pressure around the rotor blade for two different azimuth positions obtained using the SAS model. Additionally, the results of static pressure for the SAS turbulence model are compared with the results for the RNG k-ε model – Figures 8 and 10. The results of static pressure for the SST k-ω model are not presented here because for this turbulence model only 2D model of VAWT was considered. As can be noticed, with similar values of aerodynamic loads, differences in pressure distributions for the SAS and the k-ε models are very small (Figures 5, 7 and 8). At the azimuth of 140deg, the SAS model presents a sudden drop in pressure on the outer edge of the blade in comparison to the RNG k-ε turbulence model. Based on the results obtained for the SAS model, it has been found that for azimuth between 120 and 140 degrees fluid begins to flow at the trailing edge of the blade from the outer edge of the blade towards the inner edge. This cause additional vortices, which occur on the inner edge of the blade.
To better understand the nature of flow around the one-bladed rotor of the Darrieus-type wind turbine, vorticity analysis is presented. Figures 11-13 present iso-surfaces of the spanwise vorticity for the azimuths of 0, 80 and 180 degrees using the SAS model. The values of displayed spanwise vorticity are five times smaller than the angular velocity of the rotor in order to present vorticity in the rotor size. In these figures, using different colors, vorticity of the same value but with opposite directions are shown. Additionally, for comparison, Figure 14 shows iso-surfaces of the spanwise vorticity for azimuth of 180deg for the RNG k-ε turbulence model. During the studies, using the SAS turbulence model, it was found that blade-wake interactions occur at two locations: for the azimuth of about 0deg and for the azimuth in the range of 190 to 240deg. The most visible is the blade-wake interaction in the second location (azimuth between 190 and 240deg). This interaction is caused by pressure drop on the outer edge of the blade and evolution of vortices that creates in a narrow range of azimuth between 120 and 140 degrees. These vortices move with the fluid and develop. However, the tangential velocity of the blade is much higher than a velocity of undisturbed flow and, therefore, at an angle of about 190 degrees the blade interacts with wake vortex, which was left by in the previous circulation. The blade-wake interaction is also associated with a decrease of a tangential force (Figure 5).
Figures 15 and 16 present the velocity wake one rotor diameter downstream from the rotor’s axis of rotation computed using two turbulence models – the RNG k-ε model and the SAS model at azimuth of 30 deg and 210 deg. Non-dimensional velocity $u$ is defined as $u = V_x/V_0 - 1$, where $V_x$ is the local component of fluid velocity parallel to the direction of the undisturbed velocity $V_0$. The results are compared with the experimental results of Strickland et al. [9]. The number of check points taken during the experiment measuring the $V_x$ velocity is too small in order to assess which of the turbulence model is better. Wake profiles computed using the SAS turbulence model are less smooth than those computed using the RNG k-ε turbulence model. This is because the SAS model resolves many more small scales of the flow compared to the RNG k-ε model.

Using the SAS turbulence model, two series of wake profiles are illustrated in Figures 17 and 18. These two series correspond to the two azimuth positions of the rotor: 30deg and 210deg. Velocity profiles are taken for four $x/D$ locations behind the rotor (see Figure 1). As it can be seen from the figures, the smallest drop in the wake velocity is observed at the location $x/D=0$ and with the increasing distance downstream from the rotor the wake deficit is higher. However, velocity profiles are similar at locations $x/D=1$ and $x/D=2$. It confirms the observations of Paraschivou [9].
6. Conclusions

The main objective of this research is the analysis of aerodynamic blade loads and aerodynamic wake for a one-bladed rotor. On the basis of numerical investigations it turned out that:

- The results of aerodynamic coefficients are satisfactory for the prevailing range of azimuth.
- The SAS model shows much more effects of vortex wake in the rotor area compared to the RNG k-ε turbulence model.
- Based on the CFD results and using the SAS turbulence model, the rotor consisting of one blade and operation at a tip speed ratio of 5 interacts with the vortex wake two times.
- Most likely, the results of tangential force obtained for the RNG k-ε turbulence model are too optimistic for the azimuth between 90 and 180 degrees.
- The results of aerodynamic loads are similar for the SAS turbulence models and for the SST k-ω 2D model. However, it is advisable to compare the 3D effects for these two turbulence models.
- The numerical results of wake profiles are in overall good agreement with the experiment.
- Wake characteristics behind the rotor are consistent with the experiment at the distance of one rotor diameter behind the axis of rotation.

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