Short-term dynamical evolution of grand-design spirals in barred galaxies

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ABSTRACT

We investigate the short-term dynamical evolution of stellar grand-design spiral arms in barred spiral galaxies using a three-dimensional (3D) N-body/hydrodynamic simulation. Similar to previous numerical simulations of unbarred, multiple-arm spirals, we find that grand-design spiral arms in barred galaxies are not stationary, but rather dynamic. This means that the amplitudes, pitch angles, and rotational frequencies of the spiral arms are not constant, but change within a few hundred million years (i.e. the typical rotational period of a galaxy). We also find that the clear grand-design spirals in barred galaxies appear only when the spirals connect with the ends of the bar. Furthermore, we find that the short-term behaviour of spiral arms in the outer regions ($R > 1.5$–$2$ bar radius) can be explained by the swing amplification theory and that the effects of the bar are not negligible in the inner regions ($R < 1.5$–$2$ bar radius). These results suggest that, although grand-design spiral arms in barred galaxies are affected by the stellar bar, the grand-design spiral arms essentially originate not as bar-driven stationary density waves, but rather as self-excited dynamic patterns. We imply that a rigidly rotating grand-design spiral could not be a reasonable dynamical model for investigating gas flows and cloud formation even in barred spiral galaxies.

Key words: method: numerical — galaxies: kinematics and dynamics — galaxies: spiral — galaxies: structure

1 INTRODUCTION

Spiral arms in disc galaxies can be classified into three categories: grand-design, multiple-arm, and flocculent spirals (Elmegreen & Elmegreen 1987). Grand-design spiral arms are large-scale coherent, symmetric, two-armed patterns (e.g. NGC 628), whose number fraction is more than 50% in nearby spiral galaxies (Grosbøl et al. 2004; Kendall et al. 2011). Observations show that grand-design spirals are associated with bars or companions (Kormendy & Norman 1977; Seigar & James 1998; Kendall et al. 2011), suggesting that a bar or companion is essential in forming a grand-design spiral in a disc galaxy. In barred spiral galaxies, the grand-design spirals extend from the ends of the bars. Furthermore, although some studies found little or no correlation between bar strengths and spiral arm strengths (Durbala et al. 2009; Kendall et al. 2011), other studies have found correlations (Block et al. 2004; Salo et al. 2010). These observations, therefore, suggest that bars drive grand-design spirals with the same pattern speed as the bars.

This ‘bar-driven spiral hypothesis’ has been promoted by the ballistic closed-orbit theory, which is based on non-self-gravitating hydrodynamic simulations in fixed barred potentials (e.g. Sanders & Huntley 1976; Sanders 1977; Huntley et al. 1978; Sormani et al. 2015). This theory explains the physical mechanism responsible for the formation of the spirals in barred galaxies in terms of closed orbits of the gas (see also Wada 1994): the spiral arms in barred galaxies are regarded as kinematic density waves (i.e. crowding of gaseous closed orbits) driven by an external barred potential. However, spiral arms in observed barred galaxies are composed of not gas but stars; therefore, theories based on stellar dynamics are required for investigating the origin of spiral arms in barred galaxies.

On the other hand, the ‘invariant manifold theory’ is another bar-driven spiral theory (Romero-Gómez et al. 2000; 2007; Athanassoula et al. 2009a, 2010) and has been developed from stellar orbital theories in fixed barred potentials (Danilx 1964). Essentially, the back-bones of barred spirals are bunches of untrapped stars escaped from unstable Lagrangian points $L_1$ and $L_2$ close to the ends of the bar. This means that stars should move along the arms rather than across the arms (Athanassoula 2012). This behaviour...
is completely different from the quasi-stationary density wave theory, which predicts that stars should traverse the arms but would stay longer in the arm than in the inter-arm region [Lin & Shu 1964]. Furthermore, the manifold theory predicts a rigidly rotating spiral arm with a similar pattern speed to that of the bar (i.e. $\Omega_{\text{spiral}} \simeq \Omega_{\text{bar}}$) and that stronger bars should have more open spirals compared to weaker bars [Anathassoula et al. 2009b]. Recently, Struck (2013) extended the classical epicyclic orbit approximation to the ‘p-ellipse’ orbit approximation (Struck 2006) and proposed that ensembles of eccentric resonant orbits excited in Lindblad zones can provide a backbone for generating kinematic bars and spiral waves. Furthermore, Struck (2013) showed that some resonant eccentric orbits have a similar appearance to invariant manifold orbits.

The manifold theory and eccentric resonant orbits theory, however, do not consider the self-gravity of stars, despite the fact that the self-gravity of stellar discs plays an essential role in the dynamical evolution of spirals via the (non-linear) swing amplification mechanism [Sellwood & Carlberg 1984, Carlberg & Freedman 1985, Fujii et al. 2011, Baba et al. 2013, D’Onghia et al. 2013, D’Onghia 2014]. The swing amplification mechanism, proposed by Toomre in 1981, operates through a combination of three aspects, i.e. the shearing flow, epicyclic motions, and the disc self-gravity, in disc galaxies. Because the amplification is most efficient around the corotation radius (e.g. Shu 1992), prominent spiral arms tend to have differentially rotating patterns, which almost follow the galactic rotation at every radius ($\Omega_{\text{spiral}} \simeq \Omega$; Baba et al. 2013). Besides, the pitch angles are expected to depend on the shear rates of galactic discs [Fuchs 2001, Baba et al. 2013, Michikoshi & Kokubo 2014].

For investigating the origin of grand-design spirals in barred galaxies, N-body and N-body/hydrodynamic simulations are required, and several preliminary numerical studies have been proposed. However, the studies have not reached a consensus about the dynamics of barred spirals. Some numerical simulations of barred spiral galaxies have shown that the bar and spiral arm are rigidly rotating patterns with different pattern speeds, and they are independent patterns [Sellwood & Sparks 1988, Rautiainen & Saitoh 1999] or are coupled via non-linear interactions [Masset & Tagger 1995, Rautiainen & Saitoh 1999].

1 In general, the word stationary or steady means ‘not moving.’ However, in this context, this word indicates that density waves do not propagate radially and that instead they propagate azimuthally with a single pattern speed. See Bertin & Lin (1999) for further discussion on the concept of quasi-stationary density waves.

2 The term ‘swing amplification’ is used to express the amplification process, which combines the shearing flow, epicyclic motions, and disc self-gravity, regardless of whether the process is a linear or nonlinear phenomenon. Originally, the ‘swing amplification’ and its feedback cycle were based on the linear perturbation analyses of local shearing sheets [Goldreich & Lynden-Bell 1962, Julian & Toomre 1966, Toomre 1981], and previous N-body simulations of galactic discs partly supported this mechanism [Carlberg & Freedman 1984, Fujii et al. 2011]. However, N-body simulations of galactic discs suggested the importance of nonlinearity, such as mode-mode coupling and radial migration of stars [Baba et al. 2013, D’Onghia et al. 2013], in the dynamical evolution of spiral arms.

Recently, Roca-Fàbrega et al. (2013) performed N-body simulations of pure stellar barred spiral galaxies and analysed the spiral rotation frequency from selected snapshots where the spiral amplitude is above 70% of the maximum amplitude; they concluded that the spiral rotation frequency approaches the bar’s rigid body rotation in barred galaxies with the increment of bar strength. On the other hand, Baba et al. (2013) performed N-body/hydrodynamic simulations of a barred spiral galaxy and suggested that the spiral arms are not rigidly rotating patterns but transient recurrent patterns (i.e. dynamic spirals), and these results are similar to those obtained from multiple arm spiral galaxies [Sellwood & Carlberg 1984, Fujii et al. 2011, Wada et al. 2014, Grand et al. 2012a, Baba et al. 2013, D’Onghia et al. 2013]. Grand et al. (2012a) also found that spiral arms in barred galaxies are dynamic patterns whose rotation frequencies decrease with the radius in such a way that the rotation frequency is similar to the rotation of stars.

In this study, to address the short-term (e.g. a few hundred million years) behaviour of grand-design spirals in barred spiral galaxies, we performed a three-dimensional (3D) N-body/hydrodynamic simulation of a Milky-Way-like barred spiral galaxy. This paper is organized as follows. We describe the galaxy model and our numerical simulation methodologies in Section 2. In Section 3, we present our results concerning the short-term behaviour of grand-design spirals in the barred galaxy and effects of the bar on spiral dynamics. Finally, we summarize our results in Section 4.

Long-term (e.g. $\sim 10$ Gyr) behaviour of spirals in barred galaxies, as well as effects of a ‘live’ dark matter (DM) halo, will be presented in a forthcoming paper (M. S. Fujii et al. in preparation).

2 NUMERICAL SIMULATIONS AND ANALYSIS

We performed a 3D N-body/hydrodynamic simulation of a Milky-Way-like galaxy with an N-body/smoothed particle hydrodynamics (SPH) simulation code ASURA-2 [Saitoh & Makino 2009, 2010]. In this study, we focus on the dynamical evolution of spiral arms in a simulated barred spiral galaxy, while detailed studies on spatial distributions of the interstellar medium (ISM) around spiral arms as well as the structures of the ISM/clouds and their galactic environmental dependences are separately discussed in Baba, Morokuma-Matsui & Egusa (2015a) and Baba, Morokuma-Matsui & Saitoh (2015b), respectively.

2.1 Numerical methods

The self-gravities of stars and SPH particles were calculated by Tree with the GRAvity PipE (GRAPE) method [Makino 1991]. The Tree method allows us to reduce the number of particle pair interactions that must be computed by dividing the volume into cubic cells, so that particles in distant cells are treated as a single large particle centred at the cell’s centre of mass. The GRAPE tool is a special-purpose hardware for calculating gravitational forces. In this study, we used a software emulator of GRAPE, known as Phantom-GRAPE [Tanikawa et al. 2013].
Radiative cooling and heating, star formation, and stellar feedback from Type II supernovae and H$_2$ regions were also included. The radiative cooling of the gas was solved assuming an optically thin cooling function for a wide temperature range of $20 \text{K} < T < 10^6 \text{K}$ (Wada et al. 2009). Star formation from cold, dense gas and feedback models was based on the simple stellar population (SSP) approximation with the Salpeter initial mass function. These were implemented in a probabilistic manner (Saitoh et al. 2008). The H$_2$-region feedback was implemented using a Stromgren volume approach (Hopkins et al. 2012; Baba et al. 2015).

2.2 Galaxy model

We generated the initial axisymmetric model of a stellar and gaseous disc with a classical bulge embedded in a DM halo. Fig. 1 shows the initial circular velocity curves of each component in the model.

The stellar disc follows an exponential profile:

$$\rho_{\text{disc}}(R, z) = \frac{M_d}{4\pi R_d^2} \exp\left(\frac{R}{R_d}\right) \text{sech}^2\left(\frac{z}{z_d}\right),$$

where $M_d$, $R_d$, and $z_d$ are the total mass, scale-length, and scale-height of the stellar disc, respectively. Using Hernquist’s method (Hernquist 1993), the velocity structure of the stellar disc in cylindrical coordinates is approximately determined by a Maxwellian approximation. We set the reference radial velocity dispersion by assuming that Toomre’s $Q$ at $R = 2.5 R_d$ equals 1.3 (see section 2.2.3 of Hernquist 1993).

The gas disc also follows an exponential profile with a total mass of $\rho_{d,g}$, scale-length of $R_{d,g}$, and scale-height of $z_{d,g}$. The gas disc was truncated at $5 R_{d,g}$. The initial temperature was set to $10^4 \text{K}$, and the initial velocity dispersion was $10 \text{km} \text{s}^{-1}$ everywhere.

The classical bulge follows the Hernquist profile:

$$\rho_{\text{bulge}}(r) = \frac{M_{b,0}}{2\pi} \frac{a_b}{r(r + a_b)^3},$$

where $M_{b,0}$ and $a_b$ are the total mass and scale-length of the bulge (Hernquist 1990), respectively. Following Widrow & Dubinski (2003), we generated the classical bulge from the distribution function with an energy cutoff (see Equation (10) of Widrow & Dubinski 2003). Here, we set $q_0$ of that equation to be 0.21.

For simplicity, we assumed the DM halo to be a static potential, whose density profile follows the Navarro-Frenk-White profile:

$$\rho_{\text{halo}}(r) = \frac{M_h}{4\pi f_c(C_h)} \frac{1}{r(r + a_h)^2},$$

where $M_h$, $a_h$, and $C_h$ are the total mass, virial radius, and concentration parameter of the of the DM halo, respectively (Navarro et al. 1997), and $x \equiv r/a_h$. As shown in Fig. 1, the contribution from the stellar disc to the total circular velocity in the galaxy model surpasses that from the DM haloes in the regions of $3 < R < 12 \text{kpc}$. In this case, the galaxy satisfies the criteria for the bar instability (Efstathiou et al. 1982) and spontaneously develops a stellar bar. Note that a static halo omits dynamical friction on the bar (e.g. Debattista & Sellwood 2004).

![Figure 1. Initial circular velocity curves of each component of the galaxy.](image)

Athanassoula & Misiriotis (2002); however, dynamical friction will be weak because the central density of the DM halo in this study is low. We will investigate effects of a ‘live’ DM halo on the dynamical evolution of barred spirals in a future study.

The initial numbers of stars and SPH particles were 6.4 million and 4.5 million, respectively, and the particle masses of stars and SPH particles were about $9.1 \times 10^5 \text{M}_\odot$ and $3 \times 10^6 \text{M}_\odot$, respectively. We used a gravitational softening length of 10 pc. Following the above procedures, we generated a galaxy model in a near-equilibrium state and then subsequently allowed the galaxy to evolve for $\sim 10 - 20$ rotational periods under the constraint of axisymmetry (McMillan & Dehnen 2007; Fujii et al. 2011). This equilibrium state was used as the initial condition for the numerical simulation.

2.3 Quantification of spiral arms

The quantities that characterize the spiral structure are the number of spiral arms, their shape (i.e. logarithmic, hyperbolic, segments of lines), and their amplitude (or arm-to-inter-arm contrast). In order to analyse these quantities, we used the one-dimensional (1D) Fourier decomposition method with respect to the azimuthal direction (see Rix & Zaritsky 1994). More specifically, we divided the stellar surface density $\mu(R, \phi)$ into strips using a polar coordinates $(R, \phi)$ and then performed a 1D Fourier decomposition of the each strip with respect to the azimuthal direction:

$$B_m(R) = \int_{-\pi}^{\pi} \frac{\mu(R, \phi)}{\bar{\mu}(R)} \exp(-im\phi) d\phi,$$

where $\bar{\mu}(R)$ is the azimuthally averaged surface stellar density at radius $R$, and $B_m(R)$ denotes a complex amplitude of the $m$-th mode.

Radial profiles of the pitch angle were calculated using radial changes of phases of $B_m(R)$. If we define the phase as $\phi_m(R) = \arctan(B_m/|B_m|)$, then we can evaluate the pitch angle at radius $R$ using the following equation:

$$\cot \theta_p(R) = \frac{d\phi_m(R)}{dR}.$$
We analysed the angular speeds of the spiral arms with the Fourier density peak method. In this method, the rate of angular phase changes of $B_m$, $\Omega_{\text{phase},m}(R, t)$, is referred to the ‘angular phase speed’ (Wada et al. 2011; Baba et al. 2013; Roca-Fàbrega et al. 2013).

3 RESULTS AND DISCUSSION

We present the results of the dynamical evolution of barred grand-design spirals. Fig. 4 shows the time evolution of the stellar mass distribution over a period of 1.0 – 3.4 Gyr. The simulated galaxy has an $m = 2$ grand-design spiral without a stellar bar until $t \approx 1.2$ Gyr, begins to show bar instabilities around $t \approx 1.3$ Gyr, and then reaches a quasi-steady state until $t \approx 2$ Gyr. As shown in previous numerical simulations, we confirm that the grand-design spiral is neither steady nor always connected with the stellar bar. For example, the $m = 2$ grand-design spiral is clear at $t = 2.0$ Gyr, becomes faint at $t = 2.1$ Gyr, and appears clearly again at $t = 2.2$ Gyr. This unambiguously shows that grand-design spirals change their strengths with a period of about 200 Myr.

In the following subsections, we first describe the short-term (i.e. $\lesssim 200$ Myr) behaviour of grand-design spirals and compare these results with the predictions from the swing amplification and invariant manifold theories.

3.1 Short-term behaviour of grand-design spirals

The left panels in Fig. 3 shows the time evolution of the spiral arms in the polar coordinates $(R, \phi)$ from 2.70 – 2.84 Gyr. This span corresponds to one cycle of a bar-spiral connection event. During this term, the bar and strong grand-design spiral appear at $t \approx 2.76 – 2.78$ Gyr. If we focus on the grand-design arm placed at $\phi = 180^\circ – 270^\circ$, we see that this arm is initially short and weak ($t = 2.7$ Gyr) and then grows into a grand-design spiral arm with winding until $t = 2.74$ Gyr.

The right panels in Fig. 3 show the time evolution of radial profiles of the amplitude ($|B_{m=2}|$), pitch angle ($i_{m=2}$), and angular phase speed ($\Omega_{\text{phase},m=2}$) of the $m = 2$ mode. We observe that, at the clear grand-design spiral phase (i.e. $t \approx 2.76 – 2.78$ Gyr), the spiral parameters are nearly constant with respect to the radius or slowly decrease from 3 kpc to the outer regions. In contrast, at the damping phase ($t \gtrsim 2.8$ Gyr), the radial profiles of all spiral parameters show radial modulations. Note that the radially changing pitch angle at the clear barred-spiral phase seems to contradict the traditional picture, where the observed geometries of spiral arms are frequently fitted by a logarithmic spiral (i.e. constant pitch angle: Kennicutt 1984; Kennicutt & Hodge 1982). However, as per recent measurements of observed spiral galaxies, the pitch angle for most galaxies decreases as the distance from the centre increases (e.g. Savchenko & Reshetnikov 2013), which is consistent with our results.

The top row in Fig. 4 shows the time evolution of the amplitudes at each radius. As described above, the amplitudes change with a period of about 200 Myr at each radius, although the amplitude at $R = 2$ kpc (i.e. the bar region) is more stable than those of the other regions. The upper horizontal axis in each panel measures the time normalized by the rotational period $T_{\text{rot}}$ at each radius. We see that the amplitude at each radius changes in time spans of 1 – 2 $T_{\text{rot}}$; that is, the grand-design spirals in barred spiral galaxies are not quasi-stationary patterns, but transient recurrent structures (i.e. dynamic spirals).

As shown in the middle row in Fig. 4 the pitch angles also change similarly, but their phases are inversely correlated with the phases of the amplitude changes. In other words, spiral arms become strong as they wind from open to closed and then become damped after reaching the maximum amplitude. Such evolutionary behaviour between $|B_{m=2}|$ and $i_{m=2}$ is clearly shown in the bottom panels in Fig. 5 which shows the values of $|B_{m=2}|$ and $i_{m=2}$ at $R = 4, 6, 8, 10$ kpc every 1 Myr. We see that, at all radii, the amplitudes are very small in leading spirals ($i_{m=2} > 90^\circ$) and tightly winding trailing spirals ($i_{m=2} \lesssim 10^\circ$), while the amplitudes are large in open trailing spirals ($i_{m=2} \approx 20^\circ – 45^\circ$).

The bottom panels in Fig. 5 clearly show such evolutionary behaviour between the phase speed and amplitude. When the phase speed at each radius is approximately equal to the galactic angular speed, $\Omega(R)$, the amplitude reaches a maximum.

Finally, we discuss the evolution of the bar. As shown in the left panels in Fig. 5 the bar with a semi-major axis of about 3 kpc is always located around $\phi = 0$ and $180^\circ$, even though its parameters show the time evolution. The pitch angles and phase speeds of the right panel in Fig. 5 show flat radial profiles at $R \lesssim 3$ kpc. In particular, at the clear grand-design spiral phase (i.e. $t \gtrsim 2.76 – 2.78$ Gyr), we can see that these flat profiles reach $R \approx 3$ kpc. As shown in Fig. 5, the amplitude and angular phase speed at $R = 2$ kpc are relatively stable, suggesting that the inner structure of the bar is steady. However, the amplitude and angular phase speed clearly change in time at $R = 3$ kpc. Such behaviour of the stellar bar is usually seen in $N$-body simulations of isolated discs (Martínez-Valpuesta et al. 2006; Dubinski et al. 2007), as well as cosmological simulations of disc galaxies (Okamoto et al. 2013).

3.2 Comparison with swing amplification theory

We compare our results with the swing amplification theory to investigate the physical origin of the short-term evolutionary behaviour among spiral parameters. Before this comparison, we briefly review the physical essence of the

3 For unbarred spiral galaxies, Sellwood & Carlberg (2014) argued that the dynamically evolving spiral patterns are attributed to the superposition of a few longer-lived waves, each of which has well-defined frequencies and shapes and survives for 5 – 10 rotations.
Figure 2. Face-on stellar mass distributions of the galaxy every 200 Myr from 1.0 Gyr to 2.0 Gyr, and every 100 Myr from 2.0 Gyr to 3.4 Gyr. The bar instability occurs around $t \sim 1.3$ Gyr. After the bar is well developed, grand-design spirals are clear around 2.0, 2.2, 2.4, 2.6, 2.8, 3.0, 3.2, and 3.4 Gyr.

swing amplification (see Dobbs & Baba 2014, and references therein for details). The swing amplification operates through a combination of the shearing flow, epicyclic motions, and disc self-gravity, which play roles in promoting or suppressing the formation of structures in disc galaxies (Toomre 1981). Since the direction of epicyclic motion of a star is the same as the direction which the spiral arm is sheared by differential rotation, stabilisation by rotation is reduced, and the perturbation can grow via the usual Jeans instability (Goldreich & Lynden-Bell 1965; Julian & Toomre 1966). As a concrete example, we consider a disc galaxy with a nearly flat rotation curve as our simulated galaxy (see Fig. 1). Because the angular speed follows as $\Omega \propto R^{-1}$, the timescale of epicyclic motion is given by

$$\tau_{\text{epi}} \equiv \frac{1}{\kappa} = (\frac{d\Omega^2}{dR} + 4\Omega^2)^{-1/2} = \frac{1}{\sqrt{2}\Omega}. \quad (7)$$

while the timescale of involvement with the spiral arm is given by

$$\tau_{\text{shear}} \equiv \frac{1}{R|d\Omega/dR|} = \frac{1}{\Omega}. \quad (8)$$

Comparing the above two time-scales, we can see that $\tau_{\text{epi}} \simeq \tau_{\text{shear}}$. The shearing motion cancels out the stabilisation effect of epicyclic motions, and thus, the structure can grow via self-gravity in a short time as compared to $\tau_{\text{epi}}$.

To compare the results described in Section 3.1 with the predictions from the swing amplification theory, we calculate the pitch angle at the maximum amplitude phase, $i_{\text{SWA}}$, expected from the swing amplification theory. Following Michikoshi & Kokubo (2014), $i_{\text{SWA}}$ is given by

$$i_{\text{SWA}} = \arctan \left( \frac{2\sqrt{4 - 2\Gamma}}{\Gamma} \right). \quad (9)$$
Figure 3. Evolution of the spiral arms and the $m = 2$ mode every 20 Myr. The first column shows the distribution of the stars in polar coordinates (i.e. $R$-$\phi$ plane). The peak phases of the $m = 2$ mode are indicated by dotted lines whose colours (rainbow) correspond to the $m = 2$ mode amplitudes. Time evolution is shown in a rotating frame of the bar with approximately 47 km s$^{-1}$ kpc$^{-1}$. The horizontal axis indicates the azimuthal angle $\phi$ [degrees], and the vertical axis denotes the galactocentric distance $R$ [kpc]. The remaining three columns (left to right) plot the amplitude $|B_{m=2}|$, pitch angle $i_{m=2}$ [degrees], and pattern speed $\Omega_{\text{phase},m=2}$ [km s$^{-1}$ kpc$^{-1}$], respectively.
where $\Gamma = -d \ln \Omega / d \ln R$ is a dimensionless shear rate. This equation predicts that $i_{\text{SWA}}$ is a decreasing function of $\Gamma$. This trend matches observations (e.g., Seigar et al. 2006) and N-body simulations of disc galaxies (Grand et al. 2013).

In bottom panels in Fig. 5 we plot the expected values of $i_{\text{SWA}}$ as shaded regions. In the outer regions at $R = 8$ kpc and 10 kpc, the peak pitch angles (around 25°–30°) of the simulations match the predictions well. Similar results have already been obtained for N-body simulations of multiple arm spiral galaxies (Baba et al. 2013). In contrast, the peak pitch angles at the inner regions (i.e. $R = 4$ kpc and 6 kpc) are somewhat larger than the predicted values due to the effect of the central bar. Furthermore, we also compare the frequency of appearance for $i_{m=2}$ with $i_{\text{SWA}}$. The top panels in Fig. 6 show that the most frequent pitch angle matches the values predicted by the swing amplification theory, except for $R = 4$ kpc.

In addition, the swing amplification theory can explain the evolutionary behaviour between $\Omega_{\text{phase}, m=2}$ and $|B_{m=2}|$ because the amplification is most efficient around the co-rotating radius (see Dobbs & Baba 2014, and references therein). In fact, the top panels in Fig. 5 show that the most frequent phase speed decreases as a function of the radius, but it is the same as or slightly faster than the galactic angular speed, except for $R = 4$ kpc. The previous N-body simulations of barred spiral galaxies have also pointed out that the spiral arms rotate with a decreasing angular rotation speed that is slightly faster than the galactic angular speed (Grand et al. 2012a). However, these studies have not been compared with the swing amplification theory.

### 3.3 Effects of the bar on spiral dynamics

In the above subsections, we presented the short-term behaviour of the grand-design spiral and showed that these results can be explained by the swing amplification mechanism.
design spirals. We investigate how the bar affects the dynamics of the grand-design spirals.

To clarify the dynamical behaviour of the bar-driven spirals, we investigate whether the inner spiral arms are consistent with the predictions from the invariant manifold theory. As described in Section 3.1, the manifold theory provides two predictions: (1) the spirals in strongly barred galaxies will be more open than those in less strongly barred ones, and (2) the spiral arms should be a bundle of orbits guided by resonant radii. Therefore, it would be interesting to further explore the orbits of stars comprising dynamic spirals due to a non-linear combination among the shearing flow, non-linear epicyclic (or p-ellipse) motions, and self-gravity (see Section 3.2). However, this orbit analysis is limited to the stars selected from a single snapshot. Therefore, it would be interesting to further explore the orbits of stars comprising dynamic spirals in numerical simulations for comparison with kinematic theories of stars to aid bar and spiral formation.

4 CONCLUSIONS AND IMPLICATIONS

In this study, we performed a 3D N-body/SPH simulation of a barred spiral galaxy with our original N-body/SPH code ASURA-2 (Saitoh & Makino 2003, 2010) and investigated the short-term evolution of grand-design spirals in barred galaxies. We summarize our main results and give implications below.
Short-term evolution of barred grand-design spirals

Figure 7. Bar amplitude $|B_{\text{bar}}|$ with respect to the spiral amplitude $|B_{m=2}|$ at $R = 4, 6, 8, \text{and } 10 \text{ kpc}$. The bar amplitude $|B_{\text{bar}}|$ is measured with the amplitude of the $m = 2$ mode at $R = 3 \text{ kpc}$. Each dot represents a value sampled every 1 Myr.

Figure 8. Bar amplitude $|B_{\text{bar}}|$ and spiral pitch angle $i_{m=2}$ at $R = 4, 6, 8, \text{and } 10 \text{ kpc}$. Each dot represents a value sampled every 1 Myr.

Figure 9. Motion of selected star particles with respect to the rotating frame of the stellar bar. The star particles are selected from the particles associated with a grand-design spiral at $t = 2.78 \text{ Gyr}$. Time evolution is shown in a rotating frame of the bar with approximately $47 \text{ km s}^{-1} \text{ kpc}^{-1}$. 
Figure 10. (a) Sample of the orbits of the stars shown in Fig. 9. Time evolution is shown in a rotating frame of the bar at approximately $47 \, \text{km} \, \text{s}^{-1} \, \text{kpc}^{-1}$. (b) Time evolution of the radii of the stars shown in panel (a). (c) Probability distribution of the radial migration $\Delta R$ [kpc] of the stars shown in Fig. 9. Here, $\Delta R \equiv \bar{R}_2 - \bar{R}_1$, where $\bar{R}_1$ and $\bar{R}_2$ are the time-averaged radii of stellar orbits at $2.5 < t < 2.8 \, \text{Gyr}$ and $3.0 < t < 3.3 \, \text{Gyr}$, respectively.

(i) As suggested by previous simulations (e.g. Sellwood & Sparke 1988, Rautiainen & Salo 1999), clear grand-design spirals in barred galaxies appear only when the spirals connect with the ends of the bar. This implies that barred galaxies with spirals not starting from bar ends will have weaker spirals than those in barred galaxies with spirals starting from the bar ends. Actually, some barred spiral galaxies exhibit a clear bar–spiral phase differences (e.g. NGC 3124 and NGC 3450, Baba et al. 2007) and their spirals are not clear grand-design spirals. Yet, this is not a statistical argument. To confirm our implication, it requires a statistical comparison between barred spirals with and without the bar–spiral phase difference.

(ii) Grand-design spiral arms in a barred galaxy are not rigidly rotating patterns but rather differentially rotating dynamic patterns, as suggested by previous simulations (Baba et al. 2009, Grand et al. 2012a). This means that the amplitudes, pitch angles, and phase speeds are not constant, but change within a time span of 1–2 rotational periods at each radius. Such behaviour suggests that the assumption of rigidly rotating grand-design spirals is not necessarily reasonable for investigating gas flows and cloud formation in barred spiral galaxies. This point will be discussed further in Baba, Morokuma-Matsui & Saitoh (2015b) and a forthcoming paper (Baba et al. in preparation).

(iii) The stellar bar affects the evolution of spiral arms within 1.5–2 bar radius, and this radius is consistent with observations of barred spiral galaxies (Salo et al. 2014). Within this radius, as predicted from the invariant manifold theory (e.g. Athanassoula et al. 2009a), low pitch angle spirals are lacking for stronger bars, although there is considerable scatter for weaker bars in the bar amplitude–spiral pitch angle plane. In addition, motions of stars located at a grand-design spiral are not simply consistent with the prediction from the invariant manifold theory.

(iv) The swing amplification theory can explain the most frequent pitch angles and the amplitude–pitch angle relationships in the outer regions (i.e. $R > 1.5$–2 bar radius). These results imply that interplay among the galactic shear motion, epicyclic motion of stars, and self-gravity of stars is an essential factor for the dynamics of spiral arms even in barred spiral galaxies. Note that we assumed that the DM halo is a fixed external potential, so that the bar is formed via bar instabilities in massive discs (Ostriker & Peebles 1973, Efstathiou et al. 1982). In this case, the self-gravity of the disc plays a role in the formation of spiral arms via the swing amplification. Considering a ‘live’ DM halo, however, Athanassoula (2002) showed that bars can develop even in less massive discs. We infer, then, that the spiral arms in such discs may show different behaviour from those in massive discs such as those investigated in this study. This topic will be the subject of future work.

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