Strain-Tuned Structural, Mechanical and Electronic Properties of Two-Dimensional Transition Metal Sulfides ZrS2: A First Principles Study

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Strain-Tuned Structural, Mechanical and Electronic Properties of Two-dimensional transition metal sulfides ZrS$_2$: A First Principles Study$^1$

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ABSTRACT

Two-dimensional semiconductor material zirconium disulfide (ZrS$_2$) monolayer is a new promising material with good prospects for nanoscale applications. Recently, a new zirconium disulfide (ZrS$_2$) monolayer with a space group of 59\_Pmmn has been successfully predicted. Using first-principles calculations, this new monolayer ZrS$_2$ structure is obtained with stable indirect band gaps of 0.65 eV and 1.46 eV at the DFT-PBE (HSE06) functional levels, respectively. Strain engineering studies on ZrS$_2$ monolayer show effective band gap modulation. The bandgap shows a linear regularity from narrow to wide under applied stresses (strain ranged from -6% to +8%). Young's modulus of elasticity of ZrS$_2$ rectangular cells along the tensile directions (x-axis and y-axis) is 83.63 (N/m) and 63.61 (N/m) with Poisson's ratios of 0.09 and 0.07, respectively. The results of carrier mobility show that the electron mobility along the y-axis can reach $1.32 \times 10^3$ cm$^2$/Vs. Besides, the order of magnitude of the light absorption coefficient in the ultraviolet spectral region is calculated to reach $2.0 \times 10^5$ cm$^{-1}$ for ZrS$_2$ monolayers. Moreover, by regulating the bandgap under stress, some bandgaps of the stretched energy band exceed the free energy of 1.23 eV and possess a suitable energy band edge position. The results indicates that the new two-dimensional Pmmn-ZrS$_2$ monolayer is a potential material for photovoltaic devices and photocatalytic water decomposition.

KEYWORDS: Zirconium Disulfide; Mechanical anisotropy; Stress-tuned bandgap; Carrier mobility; Optical absorption coefficient

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1. INTRODUCTION

Since the preparation of graphene[1] by laboratory exfoliation in 2004, two-dimensional materials have become a popular research area in the last decade or so. Currently, two-dimensional materials have great research potential in the direction of electronic components due to their inherent lightweight (low-dimensional) and high-performance (quantitative) characteristics. Besides, low-dimensional materials such as the hexagonal structure of graphene[2, 3] or one-dimensional carbon nanotubes have shown excellent performance in electronics, mechanics, and optics, prompting more in-depth research[4]. Of course, the two-dimensional materials themselves have some defects, such as the inherent zero bandgap of graphene, which greatly limit their practical application value. Therefore, the search for new 2D materials toward more directions and the analysis of their electronic, mechanical as well as optical properties create possibilities for improving the performance of 2D materials[5-9].

Research on transition metal disulfides began with bulk materials[10] in the fields of electronics, optics, mechanics, chemistry, and catalysis. In recent years, the direct bandgap of the material's elemental family, unique electronic structure, and high species diversity have led to increasing investment in related research[11-15]. Two-dimensional Transition-Metal Dichalcogenides (TMDCs) have a chemical structure in the form of MX\(_2\), forming a monolayer compound with multiple atomic layers, known as a pincer or sandwich structure. Most of these compounds have semiconductor properties. In recent years, typical two-dimensional semiconductor materials based on TMD-based monolayers, such as MoX\(_2\)[16, 17] and WX\(_2\)[18], have shown great potential for applications in optoelectronic devices due to their inherent wide bandgap and excellent electronic properties.

In 2011, an experimental synthesis of a new two-dimensional TMD, the ZrS\(_2\) monolayer has been reported by Zeng et al. [9] In 2014, Li et al. [19] systematically explored the elastic, electronic and optical properties of a D\(_{3d}\) point-group symmetric ZrS\(_2\) monolayer using properties of the density functional theory. They showed that 2D ZrS\(_2\) is an indirect semiconductor material indicates a band gap of 1.12eV(1.93eV)
calculated by DFT-PBE (HSE06) method which can be modified by imposing an external strain. Recently, a new two-dimensional orthorhombic structure of monolayer ZrS$_2$[20] with a space group of 59\_Pmmn was theoretically proposed and researchers calculated this new two-dimensional structure with a tunable indirect band gap, which we will subsequently investigated in more depth.

In this work, we systematically investigated the electronic, mechanical and optical properties of the new 2D orthorhombic structure of ZrS$_2$ monolayer with a space group of 59\_Pmmn by first principles calculations, in which the carrier mobility of ZrS$_2$ monolayers is further calculated by strain regulation. An applied strain offers a novel way of modifying the band gaps of ZrS$_2$ monolayer over a wide range. The energy band (PBE and HSE06 calculations) under the stress of the deformation from -6\% to +8\% were obtained by strain engineering to fit and calculate the monolayer ZrS$_2$ transformation situation, and then the carrier mobility of electrons and holes in different directions (x-axis and y-axis) were further obtained by using the elastic constants. The optical absorption coefficients were proposed, and the energy values at the edges of the energy band after subtracting the vacuum energy level were larger than the water oxidation, which predicts that monolayer ZrS$_2$ has a good potential application for photocatalytic water decomposition.

2. METHODS

The First-principle calculations are performed using the plane wave technique in the Vienna ab initio simulation Package (VASP) [21]. The ion-electron interactions are described by the projector-augmented-wave (PAW) pseudopotentials[22, 23]. The electron exchange-correlation function is treated using the generalized gradient approximation (GGA) in the form proposed by Perdew, Burke, and Ernzhof (PBE) [21, 24]. In all calculations, the energy cutoff for the plane wave is set to 550 eV. The convergence threshold is set to $10^{-6}$ eV of energy. When the magnitude of the force acting on each atom in the cell is reduced to less than 0.001 eVÅ, we consider that the atoms in the cell have reached a position of complete relaxation. A thicker 20 Å vacuum
layer was added along the z-direction to avoid the effect of interactions with neighboring layers. A 17 × 17 × 1 Monkhorst-Pack $k$-point grid is used for geometric optimization and calculation of electronic properties.

3. RESULTS AND DISCUSSION

3.1 Geometric construction

![Fig.1](image1.png)

**Fig.1** The atomic structure of ZrS₂, Top (a) and side (b) views of the unstressed optimized cell structure. Blue and yellow balls represents Zr and S atoms, respectively.

**Table 1** The calculated lattice parameters (lattice constant $a$, $b$; bond length for Zr-S; Atomic layer S-S and Zr-S distance; angles of Zr-S-Zr, S-Zr-S).

| Unit cell type | $a$ (Å) | $b$ (Å) | $l_{Zr-S}$ (Å) | $\Delta_{S-S}$ (Å) | $\Delta_{Zr-S}$ (Å) | $\angle_{Zr-S-Zr}$ | $\angle_{S-Zr-S}$ |
|----------------|---------|---------|----------------|-------------------|-------------------|-------------------|-----------------|
| ZrS₂           | 3.67    | 6.49    | 2.55           | 2.89              | 0.97              | 96.71°           | 83.29°          |
|                |         |         | 2.60           |                   |                   | 89.91°           | 82.42°          |
|                |         |         |                |                   |                   | 132.61°          | 74.10°          |

The optimization results of the monolayer $Pmmn$-ZrS₂ structure are shown in Fig. 1 and Table 1. The geometric structure of the form top and side views of ZrS₂ is presented in Fig.1(a) and (b). As shown in Figure 1, in the ZrS₂ monolayer, the zirconium and sulfur atoms are arranged with a pleated monolayer structure each Zr atom forms four Zr-S bonds with the four adjacent S atoms. In the top view, ZrS₂ shows
a graphite-like layered structure with zirconium and sulfur atoms forming a fastened hexagonal network. While from the side view, the layered structure follows the S-Zr-S sandwich. Zirconium atoms are not aligned neatly but are arranged in a wavy layer on the middle atomic plane.

As shown in Table 1, the two dimensional $Pmnm$-$ZrS_2$ structure with lattice parameters of $a=3.67\,\text{Å}$, $b=6.49\,\text{Å}$ was obtained. In the ZrS$_2$ monolayer, the zirconium atom is 2.55Å away from one of the sulfur atoms and 2.60 Å away from the other sulfur atom. The vertical distance between the two layers of sulfur atoms is 2.89 Å, and the vertical distance between the sulfur atomic layer and the nearest zirconium atomic layer is 0.97 Å. The Zr-S-Zr angle has two different values of 96.71° and 89.91°, and the S-Zr-S angle has four different values of 83.29°, 82.42°, 132.61° and 74.10°, which is consistent with the previous research[20].

3.2 Energy band and density of states of unstressed ZrS$_2$

![Fig.2 The PBE band structure (a) and PBE partial density of states PDOS (b) of unstressed ZrS$_2$ monolayer.](image)

To gain insight into possible electronic properties of $Pmnm$-$ZrS_2$ in band structure, the band structure and the density of states of this monolayer are computed (Fig.2). According to our calculation, the $Pmnm$-$ZrS_2$ monolayer shows a semiconducting behavior with a quasi direct band gap of 0.65eV calculated by DFT-PBE method. Due to the fact that DFT-PBE method almost underestimates the band gap, by HSE06 hybrid functional the band structure of the $Pmnm$-$ZrS_2$ monolayer was recomputed, where a modified band of about 1.46eV was obtained, which is consistent
with the previous research results (0.53eV/1.53eV for PBE and HSE06 method, respectively)[20]. And the valence band maximum (VBM) and conduction band minimum (CBM) located between the high symmetry points Y and Γ.

As shown in Figure 2, The conduction band minimum (CBM) is mainly from the contribution of Zr atoms, while the valance band maximum (VBM) mainly comes from the joint contribution of Zr atoms and S atoms. It is clear from the partial density of states (PDOS) calculations that the CBM is mainly dominated by the d orbitals of the Zr atom, with contributions from other sub-orbital and various sub-orbital of the S atom. In contrast, the VBM is mainly dominated by the d orbital of the Zr atom and the p orbital of the S atom after hybridization together, with the other orbitals of the Zr and S atoms occupying relatively small contributions.

### 3.3 Tuning electronic properties by strain

**Table 2** The values of VBM, CBM and bandgap by PBE and HSE06 methods at each strain case.

| Strains (%) | \(b\) Å | Bandgap (PBE) | Bandgap (PBE) | Bandgap (PBE) | Bandgap (HSE06) | Bandgap (HSE06) | Bandgap (HSE06) | Style |
|-------------|--------|---------------|---------------|---------------|-----------------|-----------------|-----------------|-------|
| -6          | 6.10   | ----          | 0.63          | ----          | 0.98            | 1.40            | 0.73            | indirect |
| -4          | 6.23   | 0.13          | 0.64          | 0.12          | 1.26            | 1.42            | 0.98            | indirect |
| -2          | 6.36   | 0.41          | 0.65          | 0.40          | 1.31            | 1.44            | 1.23            | indirect |
| 0           | 6.49   | 0.65          | 0.65          | 0.65          | 1.46            | 1.46            | 1.46            | indirect |
| 2           | 6.62   | 0.87          | 0.68          | 0.89          | 1.53            | 1.48            | 1.62            | indirect |
| 4           | 6.75   | 1.07          | 0.70          | 1.09          | 1.65            | 1.50            | 1.76            | indirect |
| 6           | 6.88   | 1.20          | 0.73          | 1.25          | 1.97            | 1.52            | 1.86            | indirect |
| 8           | 7.01   | 1.31          | 0.75          | 1.35          | 2.17            | 1.55            | 1.93            | indirect |

Because of the efficiency and convenience of applying stress to design and tune the electronic structure properties of two-dimensional materials[25], we further investigated the effect of strain on the band structure of ZrS₂ monolayer. We selected
one of its rectangular cells for the calculations. The PBE and HSE06 band structures of ZrS$_2$ monolayer at each strain case are shown in Fig.S1 in Supporting Information. As shown in Table 2 and Fig.3, for uniaxial tension ($x$ or $y$) and biaxial tension, the band gap of the ZrS$_2$ monolayer decreases or increases when the ZrS$_2$ monolayer is subjected to compressive or tensile strain. The compression or stretching of uniaxial tension ($x$-axis) has more influence on the bandgap than that of uniaxial tension ($y$-axis). The effect of biaxial compression or stretching on bandgap is similar to that of $x$-axis compression or stretching.

For the compression or stretching of uniaxial tension ($x$-axis), the reduction of the bandgap is accelerated as the compressive stress increases. Compared with other materials, such as silicene[26], the bandgap of ZrS$_2$ monolayer is more sensitive to changes in compressive stress, and the bandgap of ZrS$_2$ monolayer decreases faster when the compressive stress reaches 6%. When the compressive stress reaches 6%, the bandgap of the ZrS$_2$ monolayer decreases by about 0.5 eV. While the tensile stress and its band gap almost have a linear trend, and the bandgap becomes wider and wider with the increase of the tensile stress.

![Fig.3](image)

**Fig.3** Effect of strain engineering on the bandgap of ZrS$_2$ monolayer. **Fig.3**(a) shows the bandgaps for uniaxial stretching of the $x$-axis; **Fig.3**(b) shows the bandgaps for uniaxial stretching of the $y$-axis; **Fig.3**(c) shows the bandgaps for biaxial stretching.
3.4 Mechanical stability

3.4.1 Elastic coefficients

Table 3 Calculated of 4 independent elastic constants, Young’s modulus and Poisson’s ratio along the x and y directions.

| Models | C_{11} (N/m) | C_{22} (N/m) | C_{12} (N/m) | C_{66} (N/m) | Y (N/m) | ν (x-axis) | ν (y-axis) |
|--------|--------------|--------------|--------------|--------------|---------|------------|------------|
| ZrS_2  | 84.12        | 63.98        | 5.56         | 2.06         | 83.63   | 0.09       |            |
|        |              |              |              |              |         |            | 63.61      |
|        |              |              |              |              |         |            | 0.07       |

Based on the elastic solid theory[27], we then calculate the elastic constants of ZrS_2 monolayers. For two-dimensional materials, using the standard Voigt notation[28], the strain energy $U$ per unit area is denoted as[29]

$$U(\varepsilon) = \frac{1}{2} C_{11} \varepsilon_{xx}^2 + \frac{1}{2} C_{22} \varepsilon_{yy}^2 + C_{12} \varepsilon_{xx} \varepsilon_{yy} + 2 C_{66} \varepsilon_{xy}^2$$  \hspace{1cm} (1)

Where the coefficients $C_{ij}$ (included $C_{11}, C_{12}, C_{22}, C_{66}$) are the components of the in-plane stiffness tensor, corresponding to the second partial derivative of strain energy concerning strain ($C_{ij} = \left[ \frac{1}{S_0} \left( \frac{\partial^2 U(\varepsilon)}{\partial \varepsilon_i \partial \varepsilon_j} \right) \right]$), where $S_0$ is the area of the equilibrium unit cell. To guarantee the mechanical stability of the 2D materials, the elastic constants need to satisfy the Born-Huang criteria ($C_{11} C_{22} - C_{12}^2 > 0$ and $C_{66} > 0$) [30]. All the mechanical parameters listed in Table 3 indicate that the ZrS_2 monolayer is mechanically stable. The strain energy of ZrS_2 monolayer under uniaxial, shear and biaxial in-plane strain are shown in Fig.S2 in Supporting Information.
3.4.2 Anisotropy of Young's modulus and Poisson's ratio

![Fig.4](image)

**Fig.4** Young’s modulus and Poisson’s ratio of anisotropic monolayer ZrS\(_2\) in polar diagram.

In calculating Young's modulus and Poisson's ratio in different directions, we introduce angles to represent Young's modulus and Poisson's ratio in different directions. They are functions of the direction angles \(\theta\), which can be expressed as follows [30-32]:

\[
Y(\theta) = \frac{C_{11}C_{22} - C_{12}^2}{C_{22}\cos^4(\theta) + A\cos^2(\theta)\sin^2(\theta) + C_{11}\sin^4(\theta)}
\]

\[
n(\theta) = \frac{C_{12}\cos^4(\theta) - B\cos^2(\theta)\sin^2(\theta) + C_{12}\sin^4(\theta)}{C_{22}\cos^4(\theta) + A\cos^2(\theta)\sin^2(\theta) + C_{11}\sin^4(\theta)}
\]

where \(A = (C_{11}C_{22} - C_{12}^2)/C_{66} - 2C_{12}\), \(B = C_{11} + C_{22} - (C_{11}C_{22} - C_{12}^2)/C_{66}\), \(C_{ij}\) are calculated elastic coefficients and \(\theta\) is the direction angle.

From Fig. 4(a), it is easy to see that Young's modulus in the plane of ZrS\(_2\) exhibits large values of 83.63 (N/m) and 63.61 (N/m) in the \(x\)- and \(y\)-axis directions, respectively. The minimum value in the 45.2° direction is 7.82 (N/m), which indicates that Young's modulus of the ZrS\(_2\) monolayer calculated from the tensile strain exhibits anisotropy. From Young's modulus results in each direction, the monolayer ZrS\(_2\) is subjected to a certain mechanical response along the direction of the applied stress, while the response to the action in the linear direction of the non-action force is not particularly pronounced. Also, Young's modulus of ZrS\(_2\) is relatively small compared to graphene (342 N/m)[28] and MoS\(_2\) (330 N/m)[33], indicating that the ZrS\(_2\) monolayer is more stretchable and flexible, which is important for applications in the direction of electronic devices and flexible materials.
Figure 4(b) shows the Poisson's ratios in each direction of the ZrS$_2$ monolayer, which is very small in the directions along the $x$-axis and $y$-axis, being approximately 0.09 and 0.07, respectively. While the Poisson's ratio achieves maximum values in the directions of 45°, 135°, 225° and 315° to the axis, with a maximum value of about 1. This means that when the material is subjected to a certain degree of tensile deformation, the resistance to deformation along the axis is much weaker than in other directions, especially in the directions of 45°, 135°, 225° and 315° from the axis, where the resistance to deformation is the strongest. The Poisson's ratio of ZrS$_2$ monolayer is somewhat smaller compared to MoS$_2$ monolayer with $\nu=0.2$[34], which implies a higher potential for the application of ZrS$_2$ monolayer than MoS$_2$ in strain engineering applications. Graphically, the Poisson's ratio in all directions of the ZrS$_2$ monolayer resembles a four-leaf clover, similar to the butterfly-shaped Poisson's ratio of the Penta-X$_2$C family the previous report[35].

3.5 Carrier mobility

Carrier mobility is usually referred to as the overall movement of electrons and holes within a semiconductor and is an important physical measure of the performance of semiconductor devices[36-40]. Based on the deformation potential theory proposed by Bardeen and Shockley[41], the carrier mobility of two-dimensional materials can be calculated according to the following equation:

$$\mu_{2D} = \frac{e^3 C_{2D}}{\hbar k_B m^* dE_1}$$  \hspace{1cm} (4)

Where $C_{2D}$ is the modulus of elasticity of a uniformly deformed crystal, for ZrS$_2$ monolayer, the calculation results are shown in Fig.S3 in Supporting Information. Where $m^*$ is the effective mass in the direction of transmission, $T$ is the temperature, and $k_B$ is the Boltzmann constant. $E_1$ represents the deformation potential constant of the electrons located at the top of the valence band (VBM) or clustered at the bottom of the conduction band (CBM) along the direction of transmission, determined by the equation $E_1=\Delta E/(\Delta l/l_0)$, where $\Delta E$ is the change in energy of the CBM or VBM under compression or tensile strain, the calculation results of $\Delta E$ are shown in Fig.S4 in Supporting Information. $l_0$ is the energy change in the direction of transmission of the
lattice constant, $\Delta l$ is the deformation of $l_0$. $m_d$ is the average effective mass of the carriers, defined by the following equation:

$$m_d = \sqrt{m_x m_y}.$$  

Based on fitting parabolic functions of the VBM and CBM locations, the carrier effective mass of the ZrS$_2$ can be obtained from the following equation:

$$m^* = \hbar^2 \left[ \frac{\partial^2 E}{\partial^2 k} \right]^{-1}$$  \hspace{1cm} (5)

**Table 4** Calculated deformation-potential constant, 2D in-plane stiffness, effective mass, and carrier mobility along the $x$ and $y$ directions of ZrS$_2$ monolayer at 300K.

| Models | Carrier type | $m_x/m_0$ | $m_y/m_0$ | $C_x^{2d}$ (N/m) | $C_y^{2d}$ (N/m) | $E_{1x}$ (eV) | $E_{1y}$ (eV) | $\mu_x^{2D}$ (10$^3$ cm$^2$V$^{-1}$s$^{-1}$) | $\mu_y^{2D}$ (10$^3$ cm$^2$V$^{-1}$s$^{-1}$) |
|--------|--------------|-----------|-----------|-----------------|-----------------|--------------|--------------|---------------------------------|---------------------------------|
| ZrS$_2$ | Electron     | 1.22      | 0.45      | 84.72           | 63.98           | 0.96         | 2.27         | 0.42                            | 1.32                            |
|        | Hole         | -0.24     | -0.65     | 84.72           | 63.98           | -10.63       | 1.45         | 0.38                            | 1.33                            |

Table 4 summarizes all the parameters related to the carrier mobility, which are calculated based on the bottom valence band top of the conduction band along the $x$- and $y$-axis directions, respectively. The carrier mobilities of ZrS$_2$ monolayers along the $x$- and $y$-axis are calculated to be 420 cm$^2$V$^{-1}$s$^{-1}$, 1320 cm$^2$V$^{-1}$s$^{-1}$ for electrons and 380 cm$^2$V$^{-1}$s$^{-1}$, 1330 cm$^2$V$^{-1}$s$^{-1}$ for holes, respectively. For PtS$_2$ and PtSe$_2$, the obtained electron mobility along the $x$ direction are 2411.50 cm$^2$V$^{-1}$s$^{-1}$ and 1103.04 cm$^2$V$^{-1}$s$^{-1}$, whereas the hole mobility along the $x$ direction is about 136.20 cm$^2$V$^{-1}$s$^{-1}$ and 217.85 cm$^2$V$^{-1}$s$^{-1}$, respectively. Simultaneously, for PtS$_2$ and PtSe$_2$ the electron mobility along the $y$ direction is 1477.13 cm$^2$V$^{-1}$s$^{-1}$ and 1289.32 cm$^2$V$^{-1}$s$^{-1}$, while the hole mobility along the $y$ direction is 218.30 cm$^2$V$^{-1}$s$^{-1}$ and 1161.70 cm$^2$V$^{-1}$s$^{-1}$.

Although compared with the maximum carrier mobilities of $4 \times 10^5$ cm$^2$V$^{-1}$s$^{-1}$ for graphene and 200 cm$^2$V$^{-1}$s$^{-1}$ for MoS$_2$, the monolayer ZrS$_2$ has lower carrier mobility than graphene but it still has better carrier mobility. What’s more important is that monolayer ZrS$_2$ has the same characteristics as monolayer PtS$_2$ and PtSe$_2$. Large differences in the values of electron and hole carrier mobilities in different directions, which will lead to the rapid migration of photogenerated electrons and holes. And the
numerical difference between the electron and hole carrier mobilities indicates the anisotropy of hole and electron carriers, which facilitates a more efficient separation of electron-hole pairs of electrons. The difference in mobility between electrons and holes allows the monolayer ZrS$_2$ material can to be used for photocatalytic hydrolysis for a long time, maintaining the photocatalytic activity.

3.6 Absorption coefficient

From a practical application point of view, we are very concerned about the optical performance of the ZrS$_2$ monolayer. We have calculated absorption properties based on the dielectric function $\varepsilon(\omega) = \varepsilon_1(\omega) + i\varepsilon_2(\omega)$, where $\omega$ is the frequency. The absorption coefficient $\alpha(\omega)$ was calculated using: [42]

$$\alpha(\omega) = \frac{\sqrt{2\omega}}{c} \left( \sqrt{\varepsilon_1^2(\omega) + \varepsilon_2^2(\omega)} - \varepsilon_1(\omega) \right)^{1/2}$$

(6)

where $\varepsilon_1$ is the real part of the complex dielectric function, which could be obtained from $\varepsilon_2$ using the Kramer-Kronig relationship. $\varepsilon_2$ is defined as: [43]

$$\varepsilon_2(\omega) = \frac{4\pi^2 e^2}{\Omega} \lim_{q \to 0} \frac{1}{q^2} \sum_{c,v,k} 2 w_k \delta(\varepsilon_{ck} - \varepsilon_{vk} - \omega)$$

$$\times \left| \mu_{ck+e_{aq}} \mu_{vk} \right| \left| \mu_{ck+e_{\beta q}} \mu_{vk} \right|^*$$

(7)

where $\alpha$ and $\beta$ refer to the $x$ and $y$ directions, and $\Omega$ is the volume of the unit cell. The indices $c$ and $v$ refer to the conduction and valence band states, respectively. $\mu_{ck}$ corresponds to an eigenstate with wave vector $k$. 

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Fig. 5 The calculated light absorption spectra for the ZrS\textsubscript{2} monolayer.

We calculated the light absorption coefficients of ZrS\textsubscript{2} monolayer along different transmission directions (x-axis and y-axis). The spectrum transitions from the infrared region to the ultraviolet region and the overall light absorption coefficient of ZrS\textsubscript{2} monolayer material in the planar direction along the x-axis is generally larger than that of ZrS\textsubscript{2} along the planar y-axis direction. In the visible regions, the light absorption coefficients along the x- and y-axis can reach $0.5 \times 10^5$ cm\textsuperscript{-1}, but it still appear low compared to the UV region. In the UV region, the light absorption coefficient along the x-axis can reach more than $2.0 \times 10^5$ cm\textsuperscript{-1}, and the light absorption coefficient along the y-axis can also reach more than $1.25 \times 10^5$ cm\textsuperscript{-1}. Compared with the visible region, the ZrS\textsubscript{2} monolayer performs well in the UV region, which indicates that ZrS\textsubscript{2} monolayer may be a promising material for photovoltaic applications.
3.7 Band edge positions of ZrS$_2$ monolayer

![Diagram showing band edge positions]

**Fig.6** The position of the band edge of the ZrS$_2$ monolayer influenced by strain stretching.

As we know, the most important condition for a two-dimensional semiconductor material to be used for photocatalytic hydrolysis [44-46] is to have a bandgap exceeding a certain forbidden bandwidth, the theoretical value of this bandgap must be greater than the electrolytic voltage of water, 1.23 eV. In practice, the 2D semiconductor should be able to withstand a voltage greater than or equal to 1.6 eV to ensure that the photocatalytic reaction can be carried out in the visible light range. To ensure that the reduction and oxidation of water can occur, the conduction band should lie at a lower potential than the reduction potential of water (at 0V NHE pH=0) and the valence band should be higher than the oxidation potential of water.

As shown in Fig.6, we sorted out the position of the band edge of the ZrS$_2$ monolayer after stress conditioning, and the comparison with the redox potential of water shows that the bandgap width of the ZrS$_2$ monolayer 1.46eV is larger than the electrolytic voltage of water, and we obtained a wider bandgap of the forbidden band (2.17eV) by the stretching of stress. It is worth noting that the valence band top changes very slightly when stretching the ZrS$_2$ monolayer, considering the efficiency of the actual water decomposition, so the potential of the conduction band bottom cannot be too high. It is easy to see from Fig. 6 that the conduction band bottom and valence band
are more symmetrically distributed at the more outer side of the redox potential under the condition of 2% tensile stress. ZrS$_2$ monolayer is able to regulate the bandgap by stress to reach the potential requirement for decomposition, then which is a promising material for photocatalytic hydrolysis.

4 CONCLUSIONS

In summary, we have verified the electronic and mechanical properties of the new configuration $Pmn$-ZrS$_2$ monolayer using first-principles calculations, confirming its stability. The bandgap of 0.65 eV was calculated by the PBE method, which largely underestimates the value of the bandgap (compared to the HSE06 method 1.46eV). Then, we applied stress to the $Pmn$-ZrS$_2$ structure, stretching it in different directions from -6% to 8% to modulate the bandgap. For $x$-axis tension, band gap data are obtained from 0 eV to 1.31 eV (PBE method), corresponding to the results of the HSE06 method from 0.98 eV to 2.17 eV. With the bang gap dates calculated by the PBE method, we obtained the parameters of the mechanical properties of ZrS$_2$ monolayers, including the elastic constants, Young's modulus, and Poisson's ratio under uniaxial stress conditions. The results show that the elastic constants of the ZrS$_2$ monolayer is relatively smaller than those of other transition metal sulfide groups, the smaller Young's modulus and Poisson's ratio indicate that ZrS$_2$ monolayer is a relatively soft two-dimensional material that can be used as an ideal material for sensors. By calculating the carrier mobility of the ZrS$_2$ monolayer, we are pleased to find that the electron and hole mobilities in the $x$ and $y$ axis are numerically different and have more pronounced differences. The value of carrier mobility along the $y$ direction reaches 1320 cm$^2$V$^{-1}$s$^{-1}$. The high carrier mobility indicates that the ZrS$_2$ monolayer is valuable for making photovoltaic materials. By calculating the light absorption coefficients in different directions, the absorption value of the ZrS$_2$ monolayer in the UV region reaches $2.5 \times 10^5$. In addition, the strain modulation makes it easier for the ZrS$_2$ monolayer to meet the conditions of hydrolytic photocatalysis at pH=0 and pH=7. This study shows that the new two-dimensional $Pmn$-ZrS$_2$ monolayer is a potential material for photovoltaic devices and photocatalytic hydrolysis.
SUPPORTING INFORMATIONS

Fig.S1 The PBE and HSE06 band structure of ZrS$_2$ monolayer at each strain case.

Fig.S2 Strain energy of ZrS$_2$ monolayer under uniaxial, shear and biaxial in-plane strain, respectively.

Fig.S3 Fit results for ZrS$_2$ monolayer with different directional elastic constants $C_{2d}$, respectively.

Fig.S4 Deformation potential constant for different directions of ZrS$_2$ monolayer, respectively.

Declarations

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Conflicts of interest
There are no conflicts of interest to declare.

Availability of data and material
N/A

Code Availability
All data, models, and code generated or used during the study appear in the submitted article.

Authors Contribution Statement
Qi Song performed the data computation, analysis and wrote the first draft of manuscript;
Xin Liu contributed to the data analysis and Program Testing;
Hui Wang contributed to the topic selection, data analysis and manuscript revision;
Xiaoting Wang helped to the manuscript preparation;
Yuxiang Ni helped perform the Program testing;
Hongyan Wang helped perform the constructive discussions.

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