Protein–Water–Ice Contact Angle

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ABSTRACT: The protein–water–ice contact angle is a controlling parameter in diverse fields. Here we show that data from three different experiments, at three different length scales, with three different proteins, in three different laboratories yield a consistent value for the protein–water–ice contact angle (88.0 ± 1.3°) when analyzed using the Gibbs–Thomson equation. The measurements reinforce the validity of each other, and the fact that similar values are obtained across diverse length scales, experiments, and proteins yields insight into protein–water interactions and the applicability of thermodynamics at the nanoscale.

INTRODUCTION

The interaction of water with proteins and other biological molecules is fundamental to biology and a subject of intense current interest.1−4 Knowledge of the contact angle that an ice–water interface makes with a protein could add new insight to this interaction. Also, the protein–water–ice contact angle is a controlling parameter in processes in diverse fields including cloud physics,5 cell and tissue cryopreservation,6,9 food processing,7 artificial snow making,8 and natural biological adaptions in cold-climate-resilient plants, animals, and bacteria.10 Even though this property can be determined indirectly from the Gibbs–Thomson equation (the thermodynamic relationship that describes freezing-point depression due to interfacial curvature), this approach requires knowledge of geometric dimensions that are difficult to estimate at the nanometer length scales associated with protein–water–ice interactions. Consequently, it is common to assume speculative values for the contact angle7,8 or to use phenomenological parametrizations that lump the contact angle with other physical properties.5,12 Specifically in the field of cryobiology, inaccurate values of the protein–water–ice contact angle may lead to errors in the prediction of intracellular ice formation temperatures or of ice-binding protein activities.

GIBBS–THOMSON EQUATION

The growth of ice in a confined space is limited by the geometrically imposed ice–liquid curvature and the ensuing freezing-point depression. See Figure 1. The relationship between freezing point depression ΔT (the amount that the equilibrium freezing point of the confined aqueous solution is below the freezing point of the unconfined aqueous solution5) and the curvature of a spherical ice front in a

Figure 1. Schematic of ice in a cylindrical confining pore. The pore diameter, d, and the ice–water–wall contact angle, θ, are identified.
freezing-point depression $\Delta T$ resulting from the constraint that ice grow through voids between adsorbed antifreeze proteins.\textsuperscript{17} See Figure 2. It is important to understand that these antifreeze proteins have a unique interaction with the ice surface that enables them to adhere to ice crystals. Whereas the ice-binding domain of the protein has a high affinity for ice over liquid water, the outward-facing domains of the protein do not have this preference for ice.\textsuperscript{11,17} Here, we consider the contact angle resulting from interactions of the water–ice interface with the nonbinding surfaces of the antifreeze protein.

If the spatial distribution of the ice-binding proteins is modeled as a Poisson point process, then the expected value of the diameter of circular voids is given by $d = 1/\sqrt{\sigma}$, where $\sigma$ is the average surface density of adsorbed antifreeze protein.\textsuperscript{21}

For protein densities that yielded mean void diameters ranging from 7 to 35 nm, the thermal hysteresis was well fit by the relationship

$$\Delta T = \frac{(4.65 \pm 0.35 \text{ nm K})}{d}$$

When this expression is substituted into eq 1, the resulting value of the protein–water–ice contact angle is found to be $87.5 \pm 0.2^\circ$. An estimate of the contact angle from a similar analysis was first published in ref 17; the value reported here differs slightly (by $\sim2^\circ$) from the value given in ref 17 because the previous calculation assumed regular spacing of the adsorbed proteins and thus applied a different form of the Gibbs–Thomson equation.

Higgins and Karlsson used high-speed imaging techniques to observe the mechanism of initiation of intracellular ice formation in pairs of genetically modified MIN6 (mouse insulinoma) cell strains, and found that intracellular freezing was preceded by a paracellular ice penetration process in which growing extracellular ice crystals inoculate pockets of supercooled solution that are trapped between apposing membranes at the cell–cell interface. See Figure 3. They observed that although the rate of incidence of paracellular ice penetration events varied by nearly an order of magnitude in the four different MIN6 strains investigated, the probability of paracellular freezing vanished abruptly at temperatures above a threshold temperature that fell within a narrow range ($-5.92$ to $-5.41$ °C) for each of the four cell strains. Following the evidence and arguments presented in ref 9, we assume that paracellular ice penetration events occur when ice grows through claudin pores that regulate the paracellular permeability of tight junction strands. Paracellular claudin pores are estimated to have diameters in the range of $0.65\sim0.8$ nm.\textsuperscript{22,23}
Substituting that value for $d$ in eq 1 along with the measured freezing-point depression for paracellular ice penetration relative to the freezing point of the unconfined aqueous solution, which was $-1.5^\circ$C, i.e.,

$$\Delta T = (5.41 - 5.92^\circ C) - 1.50^\circ C = 3.91 - 4.42^\circ C$$

(3)

we calculate a protein–water–ice contact angle of $88.4 \pm 0.3^\circ$. The value reported here is slightly different from the corresponding one previously reported in ref 9 (by $\sim 0.1^\circ$) due to improved estimates of the pore diameter and the ice–water interfacial tension value in eq 1.

Acker, Elliott, and McGann observed the spatiotemporal pattern of intracellular ice formation in monolayer cultures of Madine–Darby canine kidney (MDCK) cells and interpreted the appearance of directed wavelike patterns of ice formation as evidence of ice growth through gap junctions. See Figure 4.

They found that ice grew readily from cell to cell at $-3^\circ$C but not at higher temperatures. Because the unconfined isotonic solution produces a colligative freezing-point depression of 0.6 $^\circ$C, the gap junction channels can be assumed to have contributed a curvature-induced freezing-point depression of

$$\Delta T = 3.0 - 0.6^\circ C = 2.4^\circ C$$

(4)

When this $\Delta T$ together with a diameter for gap junction pores of 1.5 nm is used in eq 1, the protein–water–ice contact angle is found to be $88.1^\circ$. While 1.5 nm is an accepted estimate of the gap junction pore diameter in mammalian cells, 24 gap junction pore diameters have been measured to range from 0.8 to 2.4 nm. 25 Taking into account this uncertainty in the pore diameter, the contact angle resulting from this third experiment can be given as $88 \pm 1^\circ$.

**DISCUSSION AND CONCLUSION**

Herein we used the Gibbs–Thomson equation together with data from three different experiments on ice propagation through protein pores and obtained estimates for the protein–water–ice contact angle with error bounds of $1^\circ$ or less for each experiment. Significantly, all of the contact angles thus obtained agree with each other very closely, giving a contact angle of $88 \pm 1^\circ$ (in which the value and error represent the range of obtained results). We note that these experiments involve three different types of protein, in three different experiments, with three different geometries, in three different laboratories and with pore sizes spanning almost 2 orders of magnitude (0.65–35 nm). Furthermore, as the ice–water interfacial tension is the least well known constant in eq 1, performing a sensitivity analysis on the effect of varying the ice–water interfacial tension from 27 to 34 mJ/m$^2$ (the largest range supported by the different results in refs 18–20 and more than adequate to cover any temperature dependence of the interfacial tension), 18 broadens our precision of the protein–water–ice contact angle reported here only slightly, to $88.0 \pm 1.3^\circ$.

The results in this article are important for two reasons. First, the fact that the contact angle is close to $90^\circ$ indicates that the protein–water interfacial tension is very similar to the protein–ice interfacial tension, which is consistent with the known phenomenon of water structuring by proteins. 26–28 Because the precision of our reported value of the contact angle is high ($\pm 1.5\%$), it may be possible to use this parameter value to calibrate molecular dynamics simulations to gain additional insight into protein–water interactions. 29,30 Second, the high degree of consistency among our three independent contact angle estimates justifies the application of eq 1 to each of the experimental systems. Specifically, within the limits of experimental uncertainty, the contact angles obtained from the two experiments with the smallest pore sizes (in the range 0.65–2.4 nm) are in agreement with each other, and these nanoscale measurements also agree with the values found from the experiments with larger pore sizes of up to 35 nm. Inasmuch as the validity of the Gibbs–Thomson equation is not in doubt for the larger pore dimensions, the agreement among all three experimental studies suggests that eq 1 is also valid for the nanometer-scale pores. Thus, our results represent the smallest length scale to which the Gibbs–Thomson equation has found support for validity. 16,31,32

The results of our article beg the question, what is the smallest length scale at which it is possible for the Gibbs–Thomson equation to be valid? The Gibbs–Thomson equation has been previously experimentally verified for water in porous glass down to a diameter of 3.6 nm, and it was further shown that water molecules moved rather freely in pores of this dimension. 16 For systems such as water in glass with contact angles near $0^\circ$, the first limit of validity of Gibbsian composite system thermodynamics is set by the scale at which disjoining pressure, which keeps the interface from approaching the pore wall, becomes an appreciable effect. For our systems, in which the contact angle is near $90^\circ$, the interface comes straight out from the wall and disjoining pressure makes no contribution to the contact angle. The next limit of possible validity of thermodynamics occurs as the pore size approaches the molecular size and molecules are excluded.
from the pore. The effective diameter of a water molecule has been estimated to be 0.274 nm,\textsuperscript{33} meaning that our smallest pore size is only 2.4 molecular diameters across. It is therefore unlikely that agreement with the Gibbs--Thomson equation will be found with length scales any smaller than the smallest pore size in this article.

The applicability of eq 1 to nanoscale phase transformations is a testament to the careful structure of Gibbsian thermodynamics and nanoscale science.\textsuperscript{15} which, because of the prescient constructs of the Gibbs dividing surface and the Gibbs surface of tension, is valid even in systems with dimensions comparable to or smaller than the length scale of the interface effects. Thus, beyond their importance for applications in biology and cloud physics, our results are broadly significant for the fundamental disciplines of thermodynamics and nanoscale science.

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**Notes**

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(13) The origin of the Gibbs--Thomson equation merits some discussion. Thomson (Lord Kelvin) introduced the idea that interfacial curvature should cause an effect on phase equilibrium in 1871.\textsuperscript{34} However, because the concept of chemical potential was not yet known at the time, the equation appearing in Thomson’s paper is not thermodynamically correct. With the introduction of the chemical potential (1876–1878), Gibbs presented in general form all that is needed to correctly write down any condition for the thermodynamic equilibrium of a system containing a curved interface (e.g., the corrected liquid–vapor Kelvin equation,\textsuperscript{35} the solute–solution Ostwald–Freundlich equation),\textsuperscript{36–39} or the solid–liquid Gibbs–Thomson equation\textsuperscript{39–41} with eq 661 of his famous paper and the discussion that followed (i.e., the combination of chemical potential equality with the mechanical equilibrium describing the pressure difference across a curved surface with interfacial tension).\textsuperscript{41} While it was not until some years later that explicit forms of the chemical potentials of the liquid and solid phases were substituted into Gibbs’ equations to arrive at eq 1,\textsuperscript{40,41} the naming of eq 1 as the Gibbs–Thomson equation aply recognizes the significance of the early contributions.

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